Force display control system for simultaneous 3-axis translational motion in surgical training simulator for chiseling operation

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Abstract

The present study proposes an advanced force display control system for a surgical training simulator with virtual reality. In oral and orthopedic surgeries, a surgeon uses a chisel and mallet for chiseling and cutting hard tissue. To enable the representation of force sensation for the chiseling operation in a virtual training simulator, the force display device has been constructed with the ball-screw mechanism to obtain high stiffness. In addition, two-degrees-of-freedom (2DOF) admittance control has been used to react instantaneously to the impactive force caused by pounding with the mallet. The virtual chiseling operation was realized by the force display device with a single axis in the previous studies. In the current study, we propose the design procedure for the force display control system with the 2DOF admittance control approach to virtual operation in three-dimensional space. Furthermore, we propose the design method for the PD controller with imperfect derivative using frequency characteristics for the 2DOF admittance control system. The efficacy of the proposed control system is verified through the virtual experience from manipulating the chisel using the developed force display device in the current study.

Keywords: Surgical training simulator, Virtual reality, Force display device, Chiseling, 2DOF admittance control

Introduction

Surgical training simulators enhanced by virtual reality have been developed to enable surgeons to efficiently acquire and improve their surgical skills. The virtualized environment is created by vision, hearing and force sensory immersion so that the surgeons can practice surgical procedures repeatedly and safely with high realistic sensation [1–6]. In virtual training systems for soft tissue such as the brain [7], organs and so on [8–10], force display devices have used either the serial link mechanism [11–14] or the parallel mechanism [15–18]. These force display devices allow for increased responsiveness by lightening the moving parts, resulting in a precise sensation of contact with the soft tissue.

In oral and orthopedic surgeries, surgeons operate hard tissue such as bone and tooth using a drill, saw and so on. Virtual training simulators for operating with the drill [19–21] or saw [22–24] have been proposed in previous studies. Large operational forces are applied to the force display device. It is difficult to withstand such large operational forces in the force display devices of the training simulator for the soft tissue. Specifically, in surgical operation using a chisel and mallet, large impactive forces are applied for cutting and excising pieces of bones. Therefore, the force display device used the surgical operation of hard tissue has required high stiffness to withstand the impactive force. Furthermore, high responsiveness is also demanded to react...
instantaneously to the operational impactive force for representing the hard contact sensation.

In our previous studies [25, 26], the force display device was constructed using the ball-screw mechanism to achieve high stiffness, and the two-degree-of-freedom (2DOF) admittance control was proposed so that the device can react instantaneously to the impactive forces. It was verified that the reaction force by employing the 2DOF admittance control could precisely display the output of a virtual model.

In another previous study [27], the virtual model was designed to represent the chiseling operation with high realistic sensation by pounding with the mallet. This model was consisted of the spring-mass-damper system with the moving equilibrium point. The parameters in the virtual model were identified by comparing the real chiseling operation to the operational force detected by a force sensor. The efficacy of the 2DOF admittance control system used in the proposed virtual model was verified by subjective evaluation through the virtual experience to chisel the hard tissue. However, in these previous studies, the control systems for displaying the reaction force were designed only for the motion on a single axis. The force display control system should be extended to the motion in three-dimensional space. When contacting the hard tissue with a small operating force, the tip of the chisel can be moved to the surface of the hard tissue. On the other hand, it is difficult to move the tip of the chisel to different directions from the stabbing direction when stabbing the chisel to the hard tissue with a large operating force. As seen above, the motion of the chisel can be constrained depending on the situations in three-dimensional space.

Furthermore, the feedback controller in the 2DOF admittance control system was designed by the PD controller with imperfect derivative. However, the parameters in the PD controller were derived by the empirical rule. It is necessary to derive the parameters systematically.

In this study, the design method for the force display control system with the 2DOF admittance control approach to the virtual chiseling operation in three-dimensional space is proposed. In the proposed approach, the virtual model for representing the force sensation is constructed for three situations of manipulating the chisel in the air, contacting the hard tissue, and stabbing into the hard tissue. Furthermore, the design procedure for the parameters in the PD controller with imperfect derivative using frequency characteristics is also proposed for designing systematically the feedback controller with increasing a high-frequency gain and suppressing the vibrational motion. The efficacy of the proposed control system is verified through the virtual experience manipulating the force display device.

**Methods**

**Force display device**

Figure 1 shows an illustration of the force display device in the virtual surgical simulator used in the current study. Figure 2 shows the skeleton diagram of this force display device. This notation of the diagram is referred in [28]. This device has 5DOF motion, and the chisel as the end effector can move in the $x$-, $y$-, and $z$-directions and rotate in the $\phi_y$- and $\phi_z$-directions. The chiseling translational...
motions in the force display device are realized using the ball-screw mechanism (THK, SKR46). In the force display device, the ball-screw mechanism as a translational mechanism is located on the bottom as shown in Fig. 2. This mechanism whose allowable moment in the linear table is 579 Nm has more than enough stiffness to resist the maximum impactive force. The rotational mechanism is located on the edge of the device for reducing the load to it. The torque-loaded components in the rotational mechanism are designed to withstand the impactive force. These can be maintained with the deflection of less than 1 mm. The rotational mechanism is fixed rigidly to the linear table of the ball-screw mechanism. Therefore, the total stiffness of the force display device is enough to the maximum impactive force.

Table 1 shows the specifications of the force display device.

|                | Translational motion | Rotational motion |
|----------------|----------------------|-------------------|
| Display force  | Max. 100 N           | Max. 5.49 Nm      |
| Velocity       | Max. 0.76 m/s        | Max. 1181 deg/s   |
| Distance or angle | 290 mm               | 65 deg            |

The previous study [33] showed that the maximum tangential velocities of human arm were from 0.7 to 1.3 m/s. However, it is difficult to realize both of high-speed motion and large displayed force in the force display device. Therefore, we set the requirement of the maximum velocity to over 0.7 m/s in this study.

The servomotors installed into the ball-screw mechanism are MAXON EC45 on each axis. The servomotors using to the rotational mechanism are EC60flat in \( \phi \), \( \phi \), \( \phi \) -directions. The reduction gears mounted each servomotor are GP42C (3.5:1) in \( x \)- and \( y \)-directions, GP62 110499 (5.2:1) in \( z \)-direction, and GP52C (19:1)\( \phi \), \( \phi \) -directions, respectively. These specifications of the force display device satisfy to create realistic surgical sensations when using the chisel.

A six-axis force sensor (Leptino, 080YA501) is installed at the bottom of the rotational mechanism. The rated capacities of measurable force and torque are 500 N and 20 Nm on each axis, respectively. The resolutions of those are 0.125 N and 0.005 Nm, respectively. Therefore, the impactive force applied to the end effector by an operator can be measured by the force sensor. And, it
also enables to measure suitably the operational force to a lightweight object such as a chisel.

**Force display control system**

To create the force sensory immersion with high realistic sensation, the motion of the drive system requires precise tracking of the output of the virtual model. However, if the conventional admittance control, which consists of only feedback control, is applied to the force display device, the responsiveness of the force display device with the ball-screw mechanism used in the current study can be reduced by increasing the mass of moving parts.

Therefore, the 2DOF admittance control extended from the traditional admittance control system to 2DOF control approach by combining the feedforward and feedback controls [34] is applied to the drive system for instantaneously reacting and precisely tracking the output of the virtual model. The feedforward controller to control input provides instantaneous responsiveness to the drive system. And, the feedback controller enhances the tracking performance even with disturbance and modeling error of the drive system. Figure 3 shows the

![Graph showing the comparison of conventional and proposed control systems.](image)

**Table 3** Parameters on feedback controllers

| Direction | $\alpha$ | $K_P$ | $T_D$ | $\eta$ |
|-----------|----------|-------|-------|--------|
| x-axis    | 1.5      | 4.7   | 0.020 | 0.50   |
| y-axis    | 1.5      | 3.7   | 0.013 | 0.40   |
| z-axis    | 1.5      | 4.0   | 0.015 | 0.60   |

![Graph showing the Bode diagram comparison.](image)
2DOF admittance control installed in the force display device, where $F$ is the operational force measured by the force sensor, $u$ is the input command, $x_d$ is the position of the tip of the chisel and $d$ is the disturbance. The mathematical representations of each block are described in the subsections below.

**Drive system** $P_D$

The velocity feedback control is implemented into the servomotor system on each axis. We assumed that the 3DOF translational motions and the 2DOF rotational motions are controlled independently. And, the drive systems of the translational motion can be represented simply as

$$\ddot{x}_{di} = \frac{1}{T_{mi}}\dot{x}_{di} + \frac{K_{mi}}{T_{mi}}u_i, \quad (i = x, y, z),$$

where $T_m$ is the time constant, $K_m$ is the gain and $i$ is the moving direction. The time constants and the gains in the three dimensions are identified as Table 2. The force caused by the motion of other axes such as Coriolis force is not taken into consideration in this study. Because the influence of that force is small due to the small angular velocities of chisel motion, and the disturbance can be suppressed by the servo drive system.

The servomotors used in the rotational mechanism is used to display the reaction torque to rotate the chisel. The restraint in the chisel rotation caused by stabbing the chisel to the hard tissue and contacting the obstacles in the radial direction of the chisel can be realized by displaying the reaction torque. However, in this study, we focus on the design of force display control system for the translational motion of chisel operation. Therefore,

### Table 4 Comparison with gain and break frequency of feedback controller in y-axis

| Method   | Gain | Break freq. |
|----------|------|-------------|
|          | Low freq. | High freq. | Low freq. | High freq. |
|          | dB     | dB         | rad/s     | rad/s |
| Conv. [27] | 11.20  | 28.94      | 0.2941    | 0.7143 |
| Proposed  | 25.99  | 51.04      | 55.56     | 194.4  |

**Fig. 6** Bode diagram of closed-loop feedback control system from $x_{vy}$ to $x_{dy}$ in y-axis
we do not discuss the reaction torque display to the chisel rotation.

**Feedback controller $K_C$**

According to the analysis of the 2DOF admittance control system in the previous study [27], the feedback controller $K_C$ needs to increase a high-frequency gain to track the output of the virtual model precisely. Therefore, the PD control is applied to the feedback controller. Then, the derivative term in the PD controller is represented by the imperfect differential calculus to suppress the sensor noise and the vibrational mode of the device. The transfer function of the PD controller can be represented as

$$K_{C_i}(s) = \frac{U_{fb}(s)}{E_i(s)} = K_{Pi} \left( 1 + \frac{T_{Di}s}{\eta_i T_{Di}s + 1} \right), \quad (i = x, y, z),$$  

where $s$ is the Laplace operator, $K_P$ is the proportional gain, $T_D$ is the derivative time and $\eta$ is the derivative coefficient. These parameters are configured after the design of the feedforward controllers and the virtual model, as mentioned later. In the previous studies [27], the PD controller was designed using the empirical rule. In the present study, we propose the design procedure for the PD controller using the frequency characteristics. The gain plot of the PD controller is shown in Fig. 4.

In the design of the PD controller, first, the temporal proportional gain $K'_{Pi}$ is increased while the vibrational motion in the device is suppressed within the allowed amplitude, and the derivative time $T_D$ is zero as

$$\max K'_{Pi}, \quad (T_D = 0, \quad U_{di} < U_o, \quad i = x, y, z),$$

where $U_o$ is set as the allowed amplitude of vibrational motion in the position of the end effector $x_{d_i}$, and $U_d$ is the amplitude of the vibrational motion in the position of the end effector $x_{d_i}$. In the present study, the allowed amplitude $U_o$ of the vibrational motion is set as $U_o = 1$ mm to have no adverse influence on the operational sensation. To suppress the vibrational motion, which can be increased by adding the derivative term, the proper proportional gain $K_P$ can be designed as

$$K_{Pi} = \frac{K'_{Pi}}{\alpha_i}, \quad (\alpha_i > 1, \quad i = x, y, z),$$

where $\alpha$ is the reduction factor. The tracking performance of the drive system can be decreased by increasing the reduction factor $\alpha$. We recommend a small reduction factor from 1 to 2 to maintain tracking performance.

In the next step, the temporal derivative time $T'_D$ is increased while suppressing the vibrational motion under the allowed amplitude. Here, the temporal derivative coefficient is set as $\eta'_i = 1/(\alpha_i - 1)$. The break frequency over which the gain is increased is diminished by increasing the derivative time. The temporal derivative time derived in this step is represented as

$$\max T'_{Di}, \quad (\eta'_i = \frac{1}{\alpha_i - 1}, \quad U_{di} < U_o, \quad i = x, y, z).$$

Finally, the derivative coefficient $\eta$ is reduced to increase the high gain's range, and the proper derivative time $T_D$ can be obtained as

### Table 5

| Direction   | $\omega_f$/rad/s |
|-------------|------------------|
| x-axis      | 23.0             |
| y-axis      | 6.0              |
| z-axis      | 3.0              |

### Table 6

| Situation       | Model parameters | Generalized parameters |
|-----------------|------------------|-----------------------|
|                 | $m_v$/kg | $c_v$/kg/s | $k_v$/N/m | $\omega_n$/rad/s | $\alpha$ | $\omega_c$/rad/s | $K$ |
| (a) Contacting hard tissue | 100 | $1.2 \times 10^4$ | $3.6 \times 10^5$ | (a) | 60 | – | U | U U 
| (b) Manipulating in air | 2 | 20 | 0 | (b) | – | – | 10 | U |
The derivative time $TD$ varies depending on the derivative coefficient $\eta$, whereas the low break frequency does not vary according to the constraint in Eq. (6). In the present study, Table 3 shows the reduction factor $\alpha$, the proportional gain $KP$, the derivative time $TD$ and the derivative coefficient $\eta$.

Figure 5 shows the frequency characteristics of the proposed PD controller. For comparison purpose, we also show the PD controller designed using the conventional approach [27]. In this figure, the upper and lower graphs represent the gain and phase characteristics, respectively. The blue and red lines represent the characteristics of the conventional and proposed PD controllers, respectively. The low- and high-frequency gains and these break frequencies are shown in Table 4.

Figure 6 shows the closed-loop characteristics of the feedback control systems from $x_{v_y}$ to $x_{d_y}$ in the frequency domain. The arrangement of graphs is the same as in Fig. 5. The blue and red lines represent the characteristics of the conventional PD control and proposed PD control, respectively. The proposed PD control system has a higher high-frequency than the conventional PD control system. Therefore, the responsiveness of the drive system to the impactive force can be improved by the proposed PD control system.

In the design procedure of the proposed PD controller, the allowed amplitude of the vibrational motion is given as the boundary condition for suppressing the vibrational motion within 1 mm. Thus, it is difficult to increase the high frequency gain or decrease the low break frequency to the proposed PD controller as shown in Table 4. On
the basis of these results, we confirmed that the parameters in the proposed PD control were designed appropriately for tracking precisely the output of the virtual model and suppressing the vibrational motion.

**Feedforward controller as reference input, $P_V$**
The feedforward controller as the reference input to the feedback control system is constructed with the proper virtual model $P_V$ to create the appropriate chiseling environment. The virtual model $P_V$, which is the source of the force representation for creating the operational sensation, represents the dynamics relationship between the operational force and the tip position of the chisel. The dynamics of the virtual model is represented as

$$m_v \ddot{x}_v + c_v \dot{x}_v + k_v (x_v - z) = F_i + m_v \gamma g_i, \quad (i = x, y, z),$$  

where $x_v$ is the position of the tip of the chisel in the virtual model, $z$ is the equilibrium point and $g$ is the gravitational acceleration. The model parameters $m_v$, $c_v$ and $k_v$ are the mass, viscosity coefficient and spring constant in the virtual model, which are represented as the spring-mass-damper system, respectively. The design procedure of these model parameters $m_v$, $c_v$ and $k_v$ is described in the next section. The gravitational acceleration is $g_x = -9.8 \, \text{m/s}^2$ in the $x$-axis, and other axes are $g_y, g_z = 0 \, \text{m/s}^2$. However, the addition of pure gravitational acceleration in the virtual model causes the overload of the motor in the force display device. Therefore, the safety coefficient $\gamma$ is multiplied by the gravitational acceleration $g$. In the present study, the safety coefficient is set as $\gamma = 0.2$. The equilibrium point in the $x$-axis is set as $z_x = 0 \, \text{m}$.

**Feedforward controller to control input, $L_F P_V P_D^{-1}$**
The feedforward controller added to the control input of the feedback control system is constructed with the pseudo virtual model $\hat{P}_V$, the low-pass filter $L_F$ and the inverse model $P_D^{-1}$ of the drive system to improve the responsiveness of the force display system. The low-pass...
filter $L_F$ is applied in front of the pseudo virtual model to suppress the sensor noise and is represented as

$$\dot{F}_v = -\omega_f F_v + \omega_f F_i, \ (i = x, y, z),$$

where $F_v$ is the modified operational force through the low-pass filter. The low-pass filter parameter, $\omega_f$ is equal to the cut-off angular frequency. Table 5 shows the cut-off angular frequency in the filter applied to the control system on each axis. The low-pass filter was designed by making the cut-off angular frequency increase while the amplitude of the vibrational motion is suppressed with less than 1mm for reducing the signal loss of the measured forces adding to the pseudo virtual model and suppressing the vibrational motion. Therefore, the parameters in the low-pass filters were designed appropriately for getting better responsiveness of the force display device.

The pseudo virtual model $\tilde{P}_V$ in the feedforward controller to the control input is designed as

$$m_v \ddot{x}_v + c_v \dot{x}_v + F_v = F_i + m_v \gamma g, \ (i = x, y, z).$$

Since the feedforward controller to the control input is used to improve the responsiveness of the drive system and is required to avoid worsening the contact sensation on the hard tissue, the spring term has been removed from the virtual model $P_V$.

The inverse model of the drive system $P_D^{-1}$ is implemented to suppress the response lag by the drive system, and is represented as the inverse of Eq. (1).

Parameters design of virtual model

**Design of virtual model's parameters on situations**

To represent the operational sensations such as the contact with the hard tissue and manipulation of the chisel freely in the air, the model parameters $m_v$, $k_v$ and $c_v$ in the virtual model can be varied in accordance to the situations. In the situation which the chisel is in contact with the hard tissue, the model parameters can be derived by transforming the virtual model of Eq. (7) to the generalized form as

$$\ddot{x}_v + 2\zeta_i \omega_n \dot{x}_v + \omega_n^2 x_v = K_i F_i + \gamma g_i + \omega_n^2 z_i, \ (i = x, y, z),$$

Fig. 11 Experimental results using 2DOF admittance control in $y$-axis
where
\[ \omega_{ni} = \sqrt{\frac{k_{vi}}{m_{vi}}}, \quad \zeta_i = \frac{c_{vi}}{2\sqrt{m_{vi}k_{vi}}}, \quad K_i = \frac{1}{m_{vi}}, \quad \] (11)

\( \omega_n \) is the natural angular frequency, \( \zeta \) is the damping ratio and \( K \) is the gain of the virtual model. The damping ratio is given as \( \zeta = 1 \) to suppress the vibration. To represent the situation in which there is contact with the hard tissue in the virtual model, the gain \( K \) is minimized, and the natural angular frequency \( \omega_n \) is increased while they are required to satisfy \( U_{di} < U_o \) to suppress the vibrational motion.

In the situation where the chisel is manipulated in the air, the spring term is not required. Therefore, the virtual model can be represented as a first-order lag system with the integrator as
\[ \ddot{x}_{vi} + \omega_{ci}\dot{x}_{vi} = K_iF_i + \gamma g_i, \quad (i = x, y, z), \] (12)

where
\[ \omega_{ci} = \frac{c_{vi}}{m_{vi}}, \quad K_i = \frac{1}{m_{vi}}. \] (13)

To represent the situation where the chisel is manipulated in the air, the gain \( K \) is increased, and the cut-off angular frequency \( \omega_{ci} \) is decreased while satisfying \( U_{di} < U_o \) to suppress the vibrational motion.

In the current study, we designed the virtual model's parameters for each situation, as shown in Table 6. The rows (a) and (b) in Table 6 show the model parameters for representing the situations of having contact with the hard tissue in the virtual model.

**Table 7** Maximum absolute errors of positions between virtual model and drive system

| Direction | Admittance control | 2DOF Admittance control |
|-----------|--------------------|-------------------------|
| Conv. PD [27] | Proposed PD |
| x-axis | 4.11 mm | 1.70 mm |
| y-axis | 21.4 mm | 17.7 mm |
| z-axis | 34.0 mm | 16.7 mm |
the hard tissue and manipulating the chisel in the air, respectively.

**Switch of virtual model’s parameters with changing situation**

The model parameters represented in previous subsection are switched depending on the situation as shown in Fig. 7. The switch conditions of the model parameters for manipulating the chisel in the air and having contact with the hard tissue are designed independently of the translational motion of the three axes. On the other hand, to represent the situation of stabbing the tip of the chisel to the hard tissue when large operational force is applied, the virtual model is designed according to the motion of three-dimensional space. In the current study, we proposed the design procedure that enables the virtual model to represent the free manipulation sensation, contact sensation, stabbing sensation and pulling sensation created by an up-down motion.

The contact sensation on the hard tissue is created by switching the model parameters from (b) to (a) on each axis when small operational force is applied. In the situation where the operational force in the contact direction is larger than the threshold value $F_{s1}$, the stabbing sensation is created by switching the model parameters from (b) to (a) in all axes to represent the restrained situation. The pulling sensation is created by switching the model parameters from (a) to (b) when the operational force to the opposite direction is larger than the threshold value $F_{s2}$. Figure 8 shows these switching conditions of the model parameters, where $F_v$ is the modified operational force through the low-pass filter $L_F$. The boolean variable, $n = \text{true}$, indicates that the tip of the chisel is stabbing the hard tissue.

In the present study, the angle of the chisel is not considered during switching for the stabbing sensation, and the threshold values are set as $F_{s1} = 20$ N and $F_{s2} = 10$ N.

**Experimental results**

**Comparison between force display control methods**

The efficacy of the proposed 2DOF admittance control applied on each axis is verified by comparing it with the conventional admittance control [27]. Figure 9 shows
the block diagram of the conventional admittance control. The cut-off angular frequency $\omega_f$ of the low-pass filter for suppressing the vibrational motion is obtained, as shown in Table 5 on each axis. To confirm the representation of the output of the virtual model, we evaluate the error between the outputs of the proper virtual model $PV$ and the movement of the chisel through the drive system $PD$.

Figure 10 shows the experimental results using the conventional admittance control for the movement sensation in the air and the contact sensation in the $y$-axis, where (a) shows the operational force measured by the force sensor, (b) is the input command to the drive system, (c) and (e) are the velocity and the position of the tip of the chisel, respectively, and (d) and (f) are the absolute error of the velocity and the position between the virtual model and the drive system, respectively. In the free horizontal manipulation of the chisel using the conventional control approach, the maximum absolute error of the position is 0.021 m. Figure 11 shows the experimental results using the proposed 2DOF admittance control in the $y$-axis. The graphs in Fig. 11 have the same arrangement as those in Fig. 10. The absolute error of the position is less than 0.012 m.

Figures 12 and 13 show similar experimental results on the $z$-axis, whereas Figs. 14 and 15 show similar experimental results on the $x$-axis. Therefore, the proposed control system improved the realization of the virtual model for the free manipulation and the contact sensation.

Comparison between feedback controllers in 2DOF admittance control system

The tracking performance of the 2DOF admittance control with the conventional PD control [27] was compared with that of the proposed PD control using the chisel manipulation with the force display device. Figure 16 shows the experimental results by the force display device implementing the 2DOF admittance control with the conventional PD control; this figure is the results of the chisel motion on the $y$-axis. The chisel was manipulated, as described in the previous subsection. Therefore, we
refer to Fig. 11 for the experimental results of the 2DOF admittance control system with the proposed PD control. Figures 11f and 16f show that the tracking error of the conventional PD control is larger than that of the proposed PD control. Therefore, the force display device implementing the 2DOF admittance control with the proposed PD control can precisely represent the output of the virtual model.

Stabbing sensation

Figure 17 shows the experimental results of the stabbing operation using the proposed 2DOF admittance control. Graphs (a), (b) and (c) show the operational forces for operating the chisel on the x-, y- and z-axes, respectively. From 1.7 to 4 s, the tip of the chisel is in soft contact with the virtual object and can slide on the horizontal plane. From 5 to 7 s, the tip of the chisel is stabbing into the virtual object. In this situation, the operational force $F_{vz}$ is less than the threshold force $-F_{t1}$. Therefore, it is difficult to slide the tip of the chisel on the horizontal plane. After 7.5 s, the pulling sensation is created by the upward force exceeding the threshold force $F_{t2}$, and the chisel can be moved freely. It is confirmed that the proposed control system enables the representation of the stabbing and pulling sensations.

Discussion

Table 7 shows the maximum absolute errors of positions between the virtual model and the drive system in the conventional and proposed controls on each axis. The column of 2DOF admittance control shows the results of applying the conventional [27] and proposed PD controllers to the feedback control. As seen from Table 7, we confirmed that the tracking error of the chisel movement to the proper virtual model in the 2DOF admittance control with PD controller designed by the proposed approach is down by nearly half to that in the conventional admittance control. And, we could obtain the better tracking performance by designing systematically the PD controller with imperfect derivative. Therefore, the virtual chiseling experience by the force display device
could be improved by the proposed approach. Moreover, the gentle contact, stabbing and pulling sensations of the chiseling operation in three-dimensional space could be created by the proposed virtual model.

However, the tracking error of the drive system to the output of the virtual model is large in the situation of chisel manipulation in the air. Thus, the operator feels slightly heavy to manipulate the chisel in the air. A higher response will be required by the admittance control system to track precisely the output virtual model.

**Conclusion**

To virtualize the chiseling operation in the surgical training simulator in which the chisel can be used three-dimensionally, we proposed the force display device with the 2DOF admittance control system. The following conclusions are drawn from the study:

1. In the design of the feedback controller in the 2DOF admittance control system, the PD controller with imperfect derivative was designed systematically according to the frequency domain. The responsiveness of the drive system in the force display device can be improved by increasing the controller’s high frequency gain, whereas the vibrational motion in the force display device is suppressed within the allowed amplitude.
2. We proposed the virtual model of the chiseling operation in three-dimensional space that can represent the three situations of chisel manipulation in the air, contact with the hard tissue and stabbing into the hard tissue. Specifically, the stabbing situation in the proposed virtual model can represent that it is restrained to slide the chisel in the orthogonal direction to the stabbing motion.
3. In the experiments using the force display device, it was verified that the tracking performance of the drive system can be improved by the proposed 2DOF admittance control system implementing the PD controller with imperfect derivative. In addition, the soft contact, stabbing and pulling sensations of the
chiseling operation were created by the developed force display device.

In the current study, we developed the force display device for the translational chiseling operation. In future works, the rotational motion in the chiseling operation will be incorporated in the force display device. And, it is required to verify that the Coriolis force caused by the integration of translational and rotational motions can be influenced in the operational sensation.

Furthermore, to develop the surgical training simulator with high realistic sensation, it is necessary to improve the responsiveness of the drive system with respect to the force display mechanism and the control strategy.

Acknowledgements
Not applicable.

Authors’ contributions
KU, YI, YK, and YN proposed the concept of the virtual training for chiseling operation. KM and YN proposed the method to enable the virtual chiseling operation. KM carried out the development of the device, programming and experiments of this study. KU, YI, and YK supported the whole development of this study. All authors read and approved the final manuscript.

Availability of data and materials
Not applicable.

Declarations
Ethics approval and consent to participate
Not applicable.

Consent for publication
Not applicable.

Competing interests
The authors declare that they have no competing interests.

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Received: 8 May 2021  Accepted: 26 August 2021
Published online: 15 September 2021
