Strain Driven Conducting Domain Walls in a Mott Insulator

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1. Introduction

Extreme miniaturization of active electronic components, while keeping the complexity of their function,[8] has spurred much interest in low-dimensional objects, including emergent and artificially designed 2D interfaces[2,3] and flakes of 2D materials.[4,5]

For instance, naturally occurring structurally sub-nanometer adaptations are made.

Rewritable nanoelectronics offer new perspectives and potential to both fundamental research and technological applications. Such interest has driven the research focus into conducting domain walls: pseudo-2D conducting channels that can be created, positioned, and deleted in situ. However, the study of conductive domain walls is largely limited to wide-gap ferroelectrics, where the conductivity typically arises from changes in charge carrier density, due to screening charge accumulation at polar discontinuities. This work shows that, in narrow-gap correlated insulators with strong charge-lattice coupling, local strain gradients can drive enhanced conductivity at the domain walls—removing polar-discontinuities as a criteria for conductivity. By combining different scanning probe microscopy techniques, it is demonstrated that the domain wall conductivity in GaV$_4$S$_8$ does not follow the established screening charge model but likely arises from the large surface reconstruction across the Jahn–Teller transition and the associated strain gradients across the domain walls. This mechanism could turn any structural, or even magnetic, domain wall conducting, if the electronic structure of the host is susceptible to local strain gradients—drastically expanding the range of materials and phenomena that may be applicable to domain wall-based nanoelectronics.

wide interfaces, for example, domain walls, have been reported to possess the same inherent electronic response as existing circuit elements, such as switches[6] and half-wave rectifiers.[7] In addition, ferroelectric domain walls can be reconfigured in situ by a variety of external fields which can lead to exotic bulk responses. Such bulk responses offer the opportunity to both enhance existing technology (e.g., magnetoresistance,[8] colossal dielectric constants,[9] memristive behavior[10]) but also provide next generation functionality like, negative capacitance,[11] above band gap photovoltaic effects,[12] and domain wall nanoelectronics.[13] Such effects have been discussed from both a fundamental and a technological perspective in recent reviews.[14,15]

For all of these bulk responses, the key requirement is for the domain walls to exhibit a different conductivity compared to the surrounding material. Therefore, much of the research has focused on ferroelectrics as the build up of screening charges at domain walls with polar discontinuities are known to modify the local conductivity.[13,14] Examples of this, in single crystals, include BaTiO$_3$,[16] (Ca,Sr)$_3$Ti$_2$O$_7$,[17] Cu-Cl boracite’s,[18] LiNbO$_3$,[19] h-RMnO$_3$ (R representing rare earth metals),[20] and GaV$_4$S$_8$.[8]

Because of the energetically costly nature of such polar discontinuities, their spontaneous formations are normally restricted to improper ferroelectrics.[21,22] Indeed, so established is this screening charge mechanism that it is a surprise for an improper ferroelectric material, exhibiting polar discontinuities, not to have conducting domain walls.[23] In this scenario, the type of domain wall that is expected to have enhanced conductivity depends on the electronic structure of the host material: In a p-type (n-type) semiconductor the tail-to-tail (head-to-head) domain walls attract screening holes (electrons) and thus provide enhanced conductivity relative to the bulk.[24–26] The corresponding head-to-head (tail-to-tail) wall in a p-type (n-type) material is then expected to have reduced conductivity compared to the bulk.[27,28–30]

Note, in ferroelectrics, particularly thin-films, further conductivity mechanisms have been reported.[31,32] But it is challenging, especially in oxides, to disentangle intrinsic effects and those associated with, for example, enhanced defect density at domain walls[13,34] which can change surface Schottky barriers and hence conductivity.[7] There have also been reports of domain wall conductivity and even superconductivity in non-ferroelectrics. Examples of the former case include, the antiferromagnetic insulators with conducting magnetic domain

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walls—attributed to the presence of mid-gap states, or in VO₂ domain walls around the phase transition, as the new phase nucleates preferentially at ferroelastic domain walls (i.e., a metal state on heating, and an insulating state on cooling). Superconductivity has been reported to appear at structural twin walls before the bulk transition, attributed to the local symmetry of the walls and the corresponding strain coupling.

On the bulk scale it is long established that the conductivity of highly correlated systems, such as Mott insulators, can be changed by changing the inter-atomic distances. Practically, such changes to the inter-atomic distance can be achieved via applied strain, hydrostatic-, or chemical- pressures. In this work, we move these bulk concepts to the nanoscale by showing how highly conducting domain walls could be created using local strain gradients, rather than originating from the conventional screening charges mechanism. Taking the narrow band gap Mott insulator GaV₄S₈ as a representative of such highly correlated systems, we use scanning probe microscopy to reveal that the enhanced conductivity arises at domain walls which have a large surface reconstruction, a signature of local strain gradients. This mechanism explains, among other things, the origin of indistinguishable enhanced conductivities at “head-to-head” and “tail-to-tail” domain walls, which cannot be explained via the conventional screening-charge-based mechanism. Our results provide a new mechanism of generating conductivity at domain walls in single crystals, expanding the field of domain wall nanoelectronics to material systems, like Mott insulators, whose band structures are strongly influenced by strain gradients.

2. The Lacunar Spinel GaV₄S₈

For this proof-of-principle study, GaV₄S₈ is an ideal template system: it is characterized by a correlation band gap of ≈0.3 eV and has a strong charge-lattice coupling. The material crystallizes in a face centered cubic (NaCl-like) structure comprising [V₄S₄] heterocubane entities and [GaS₄] tetrahedra, as depicted in Figure 1a. In lacunar spinels, the strong charge-lattice coupling arises from the Jahn–Teller instability of the heterocubane cluster and in GaV₄S₈ this drives the ferroelectric transition.

At the Jahn-Teller transition of GaV₄S₈, taking place at TJT = 42 K, the symmetry is reduced from cubic (Fm3m) to polar rhombohedral (R3m) via an elongation of the V₄S₄ units along one of the cubic (111) directions. For the four possible domains, P₁–P₄, depicted in Figure 1b, this distortion leads to
a ferroelectric polarization of $P_z = 2.3 \mu\text{C cm}^{-2}$.[8,48] Due to the lack of ±P domain pairs, 180° domain walls of neighboring domains cannot emerge in GaV$_4$S$_8$, where the largest polar discontinuities normally occur.[10,49] The four polarization directions are illustrated schematically in Figure 1b, and the origin of the ferroelectricity is discussed in detail in refs. [8, 42] and the references therein. Below $T_{JT}$, the material undergoes a magnetic ordering at $\approx 13$ K, with several competing magnetic phases, including a Néel-type skyrmion lattice phase.[30] It is also well documented that the electronic structure of GaV$_4$S$_8$ is very sensitive to inter-atomic spacing, and can be modified with either hydrostatic,[51,52] or chemical pressure.[53]

3. Results and Discussion

To understand and correlate the local structural and electronic properties at domain walls in GaV$_4$S$_8$, we use scanning probe microscopy performed on an as-grown (111) surface of a single crystal. Figure 1c displays a representative topography image recorded at 30 K. The topography shows a large amount of surface reconstruction below the Jahn–Teller transition, which is manifested as a series of ridges and valleys that zig-zag across the surface. Using the neutron diffraction data of ref. [54], we follow the methodology of ref. [55] to calculate an expected volume strain across the transition of $-7.2 \times 10^{-4}$. We also note that the changes in topography across a phase transition can act as a reasonable proxy for the volume strains—as the AFM topography is the height/area, so a measurement of the topography is effectively a normalized value of the volume strain. A direct comparison of the topography and conductivity above and below the transition is given in Figure S1, Supporting Information, and some of the implications from such surface reconstruction are described in the Note S1, Supporting Information.

The corresponding out-of-plane piezoresponse force microscope (PFM) phase image allows us to identify these regions as different ferroelectric domains, Figure 1d. Since the image is taken on a (111) surface, the polarization of one of the four domain states, $P_1$, is perpendicular to this surface, while the polarization for the other three span 71° to the scanned surface. Hence, $P_1$ is assigned to the domain with largest amplitude in the out-of-plane piezo response, that is, the brightest areas in Figure S2, Supporting Information. Domains with lighter shades of brown correspond to domain states $P_2$–$P_4$, which can be distinguished by considering the orientation of the mechanically compatible domain walls,[56] and described for GaV$_4$S$_8$ in ref. [8]. We note, from symmetry, the need to assume the sign of the out-of-plane domain polarization, which is dictated by the type of $P43m$ inversion domain the crystal grew in: this does not affect which walls are charged, but will change the sign of the charged walls. These different polarizations are represented by the different colored crosses in Figure 1d, following the color convention of Figure 1b. Note, the PFM images show a distinct contrast at the (110)-type domain walls, which would be consistent with a strain gradient driven ferroelectric contribution, and would be a very interesting topic for future theoretical work.

The large topographic features, the ridges and valleys, clearly correlate with the ferroelectric domain structure resolved by PFM, with the largest changes in topography arising at (110)-type domain walls. From symmetry arguments these (110)-type domain walls are expected to have polar-discontinuities and consequently positive and negative bound charges. That is to say, the walls with the largest changes in topography also have polar discontinuities. We will refer to these walls as “p-type” or “n-type” when information about the charge state is important, and otherwise as “zig-zag” domain walls.

In order to see which of the domain walls are associated with increased conductivity, we collect conductive atomic force microscopy data (cAFM) (with 60 V). Figure 2a, of the region illustrated in Figure 1. In the cAFM image the bright gold colors are areas of highly enhanced current (values up to 270 nA) and the dark areas are regions of lower current. These areas of enhanced current align with the zig-zag-domain wall pattern observed in the topography and PFM images of Figures 1c,d, respectively. The observed current values, of several hundred
nanoamperes, are high for domain walls in ferroelectrics, which typically have values in the pico- to nanoamperes range.[13] One of the most striking features of the cAFM data in Figure 2 is that both the head-to-head and the tail-to-tail domain walls, which are expected to possess opposite bound charge, exhibit enhanced conductivity. From the conventional polar discontinuity argument, this would mean that “n-type” and “p-type” charge carriers have the same effects on the conductivity; in contrast to the literature on bulk GaV$_4$S$_8$.[57] This is also surprising for semiconducting ferroelectrics in general, as typically the walls with an accumulation of majority carriers are expected to have enhanced conductivity, while the walls with an accumulation of minority carriers have a reduced conductivity relative to the bulk.[3,22,27,58] In addition, if adjacent domain walls had majority p-type and n-type charge carriers, the intersection of the walls would form a depletion region. The absence of any such region in Figure 2a is inconsistent with the polar discontinuity model but consistent with the strain-gradient driven model. Note, our cAFM data sets are the same for the forward and backward scan directions, Figure S4, Supporting Information, which means the conductivity we observed is not dominated by changes to the tip-sample contact area.

To provide a more qualitative comparison between conduction and topography, we plot cross-sections of both in Figure 2b, indicated by the grey line in Figure 2a, and schematically add the topography and ferroelectric polarization vectors. We observe that large current values arise at both head-to-head and tail-to-tail domain walls, accompanied by a surface reconstruction (8h)—discussed below and detailed in Note S1, Supporting Information. The cAFM cross-section shows that the conductive regions are relatively wide, extending ≈750 nm away from the center of the wall. This non-local nature is consistent with a strain-gradient around the wall, which would effect the surrounding electronic structure of the material. However, this is inconsistent with the idea of polar discontinuity driven domain wall conductivity, as this is necessarily limited to the wall itself. For reference, in materials where the polar discontinuity driven mechanism is well established, such as the hexagonal manganites,[22,59] Cu-Cl boracite,[18] BaTiO$_3$,[60] or BiFeO$_3$[34] the walls typically have an effective electronic width of ≈100 nm.

In order to understand the correlation of topography and conductivity in GaV$_4$S$_8$ further, we consider the large surface reconstruction that arises during the Jahn-Teller transition. To represent these local strain-gradients, using an approach inspired by Aizu’s work on spontaneous strains across a symmetry lowering structural transition,[61] we compare the changes in topography relative to an assumed surface. This represents the crystal surface, had the phase transition not taken place. Practically, this is achieved by taking the square of the difference in height (8h) of the topography versus a smooth plane, schematically shown by the dashed grey line in Figure 2b. This change in height, taken along the cross-section of Figure 2a, gives an excellent correlation with the measured current (Figure 2b).

In order to visualize the topography/conductance correlation is ubiquitous over the observed area, we present 3D maps of the topography and conductivity in Figure 3. These are the same data sets provided in Figures 1c and 2a. This 3D representation shows that the large peaks and valleys in the topography along the [110]-type domain walls (orange lines) are associated with areas of enhanced conductivity (bright colors), while small changes in surface reconstruction at the [100] domain walls (such as those highlighted with blue lines) give no significant change in conductivity.

To further test the idea that the conductivity is enhanced by local strain gradient induced changes in band structure, rather than the accumulation of screening charges, we consider the system in terms of classical semiconductor–metal interface (a Schottky barrier). In a semiconductor–metal interface the conductivity depends on the respective work functions, in this case the work function of the cAFM tip (e.g., Pt-Si and BdSC-diamond) and that of the sample. Naturally, areas with p-type conductivity would have a different band structure to areas of n-type conductivity. Therefore, we performed cAFM and PFM measurements using a metallic Pt-Si tip (Figure 4) in addition to the measurements with a BdSC diamond tip (Figures 1–3). The topography of the same sample is given in Figure 4a, and the corresponding cAFM data is presented in Figure 4b. The topography shows the same structure of zig-zag-domain pattern observed in Figure 1. Two things are apparent from the cAFM: the observed current values are smaller, hundreds of picoamps compared to hundreds of nanoamps (cf., Figure 2a), and both
zig- and zag- walls have similar conductivity. This suggests that, while the tip work function changes the values of the Schottky barrier (and therefore the measured current), there is no difference in band structure between the zig- and zag- domain walls, as this would change the relative current across the domain walls. While highly problematic for the polar discontinuity driven mechanism, it is consistent with strain gradient induced changes to the band structure, as this would have carriers of the same type at both walls.

In order to identify the conductivity mechanism, we collect I(V)-spectroscopy data across zig- and zag- walls. The plotted curves in Figure 4c, for both types of tip and both types of domain wall, are the average values collected over ten data sets. The current response for each tip is the same for both types of domain walls. We fit these voltage dependent responses with the established models of conductivity in semiconductors: Schottky emission, Fowler–Nordheim tunneling, direct tunneling, thermionic-field emission, Poole–Frenkel emission, hopping conduction and space-charge-limited conduction. Following the methodology of Shih 2014, the I(V) data is plotted in a way that, if the model describes the data well, the plot will be linear. Such a linear behavior is only observed for the space-charge-limited representation of the I(V) data, Figure 4d. This does not change with different tip material. The other plots, corresponding to the different models, are given in Figure S3, Supporting Information.

To exclude the possibility that the equal conductance of zig- and zag-domain wall segments, as already observed using two types of tips, is an accident caused by a special combination of carrier densities and mobilities, we investigate the temperature dependence of the domain wall conductivity. It is established, that even in the simplest semiconducting materials, such as Si—where the electrons can be described as non-interacting particles—electrons and holes have different temperature dependent mobilities; in the case of Si, T\(^{-2.6}\), and T\(^{-2.3}\), respectively. In Mott insulators, the electrons are highly correlated and cannot be considered non-interacting. If such classical “electron” and “hole” type charge carriers could form, a difference in their respective mobilities is therefore expected. Separate cAFM line scans across a zig- and a zag- wall (see inset) were collected while cooling from 26 K to 4 K, and the data for the zig-wall is given by the waterfall plot of Figure 5a. We plot the peak values of currents from our temperature dependency for both walls in Figure 5b. The temperature dependent conductivity is indistinguishable for the two walls, except around the magnetic ordering transition, suggesting the same charge carrier type at both walls. An anomaly around the magnetic ordering is
expected, if the walls have different magnetic properties, a discussion of which is the subject of forthcoming work.

4. Discussion

The electronic properties GaV$_4$S$_8$ (as with many of the lacunar spinels$^{[13,14]}$) are governed by V$_4$ molecular clusters. Within each cluster, molecular orbitals form because of hybridization,$^{[15]}$ and so the electrons are considered to be localized on these V$_4$ molecular clusters, rather than at the atomic site, which is normally the case in Mott-insulators.$^{[16]}$ There is large distance between these clusters, 4 Å,$^{[17]}$ which only allows inter-cluster electron mobility via hoping, and serves as the origin of the band-gap.$^{[18,19]}$ Consequently, any action that causes a decrease in the inter-cluster distance, such as a compression of the unit cell in response to a spontaneous strain, is expected to dramatically increase the conductivity. Indeed, it has already been shown on bulk single crystals that external pressures drive insulator–metal transition in GaV$_4$S$_8,$$^{[16]}$ which has been attributed to changes in bond length.$^{[20]}$

Based on this, we hypothesis that the domain walls become highly conducting because the spacing between clusters decreases in response to the spontaneous strains that appear across the Jahn–Teller transition. This permits a transfer of electrons between the clusters, and hence very high levels of conductivity compared to the strain-free bulk domains. Naturally, such effects follow the strain gradients and persist away from the domain walls.

5. Conclusion

We use AFM topography images to show that a large surface reconstruction arises during the Jahn–Teller transition, which coincides with the formation of ferroelectric domain walls, identified with PFM. The corresponding cAFM images show that both the head-to-head and tail-to-tail domain walls are highly conducting compared to the bulk, and this conductivity is directly proportional to the amount of surface reconstruction squared. Such surface reconstruction is naturally associated with strain gradients, which in Mott-insulators, or any other system where the electronic structure is sensitive to strain, will change the band structure and therefore the conductivity. We substantiate the strain gradient model by noting that the temperature-dependent current response of the zig- and zag-domain walls are indistinguishable, even for cAFM tips of different work function. Furthermore, I(V)-spectroscopy identifies that the conductivity is bulk limited and well explained by space-charge-limited conductivity. This interpretation would allow any structural or even magnetic domain walls to be conducting, if the electronic structure of the host is susceptible to strain, and so significantly broadens the scope of domain wall physics by expanding the range of materials that could be used for domain wall nanoelectronics.

6. Experimental Section

GaV$_4$S$_8$ single crystals were grown by the chemical transport reactions method. As starting material for growth preliminary synthesized polycrystalline powder was used. The polycrystals were prepared by solid state reactions from the high-purity elements: Ga (99.9999%) (Alfa Aesar, Ward Hill, USA), V (99.5%) (Alfa Aesar, Ward Hill, USA), and S (99.999%) (Strem Chemicals Inc, Newburyport, USA). The iodine was utilized as the transport agent in the single crystal growth. The growth was performed at temperatures between 800 and 850 °C. Perfect truncated octahedron-like samples with dimension up to 5 mm were obtained.

The atomic force microscopy (AFM) scans were conducted on the same single crystalline sample at various temperatures using an attoAFM I (attocube systems AG, Haar, Germany) atomic force microscope with Pt-Si-tips (PtSi-FM-10, radius: 25 nm, NanoandMore GmbH, Wetzlar, Germany) as well as boron doped single crystal diamond (AD-2.8-AS, radius: 10 nm, Bruker France, Wissembourg, France) tips. Local transport data was gained by cAFM with varying dc-voltages, ranging from 1 to 60 V applied to the back electrode. PFM was conducted with the off-resonant method using frequencies ranging from 19 up to 99 kHz with 10 V excitation voltage.

Figure 5. a) Waterfall plot of the current response from 26 K down to 4 K of a zig-domain wall. The inset shows a cAFM measurement to indicate the location of the line scans for zig- (blue) and zag- (orange) domain walls, collected at 30 K. b) Temperature-dependent change in peak current values of both zig- and zag-domain walls, extracted from the waterfall plots represented in (a). The scans were done using a BdSC diamond tip.
I(V)-spectroscopy was conducted by placing a grid of measurement points over an area of interest. For each point a voltage range from 0 to 120 V (WMA-200 High voltage amplifier, Falco Systems, Katwijk aan Zee, Netherlands) was applied and the respective current signal tracked. The acquired 3D data cube was evaluated with an in-house written Matlab-script (The MathWorks, Inc., New Mexico, USA). The phase and amplitude signal of the PFM scans were measured with a lock-in amplifier SR860 (Stanford research systems, Sunnyvale, USA).

Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest
The authors declare no conflict of interest.

Author Contributions
L.Pu. recorded the scanning probe microscopy data supervised by M.A. and D.M.E. V.T. and L.Pr. have prepared the crystals. L.Pu., M.A., D.M.E., S.G., S.K., and I.K. interpreted the data and drafted the manuscript. All authors discussed the results and contributed to the final version of the manuscript.

Data Availability Statement
The data that support the findings of this study are available from the corresponding author upon reasonable request.

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