Normal and inverted hysteresis in perovskite solar cells

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Hysteretic effects are investigated in perovskite solar cells in the standard FTO/TiO2/CH3NH3PbI3–xClx/spiro-OMeTAD/Au configuration. We report normal (NH) and inverted hysteresis (IH) in the J-V characteristics occurring for the same device structure, the behavior strictly depending on the pre-poling bias. NH typically appears at pre-poling biases larger than the open circuit bias, while pronounced IH occurs for negative bias pre-poling. The transition from NH to IH is marked by a intermediate mixed hysteresis behavior characterized by a crossing point in the J-V characteristics. The measured J-V characteristics are explained quantitatively by the dynamic electrical model (DEM). Furthermore, the influence of the bias scan rate on the NH/IH hysteresis is discussed based on the time evolution of the non-linear polarization. Introducing a three step measurement protocol, which includes stabilization, pre-poling and measurement, we put forward the difficulties and possible solutions for a correct PCE evaluation.

I. INTRODUCTION

The dynamic hysteresis phenomena observed in the J-V characteristics of perovskite solar cells (PSCs) fuels an ongoing debate about its origin, accurate determination of the photoconversion efficiency (PCE), and cell stability.1–4 Several mechanisms have been proposed to explain the hysteretic behavior: ion migration,5–9 charge trapping and de-trapping,10–12 ferroelectric polarization,12–15 capacitive effects,16–18 charge accumulation at the interfaces,19, 20 or unbalanced distribution of electrons and holes.21 It is already established that the hysteresis is influenced by measurement settings such as the bias scan rate and range,3 but also by the cell pre-conditioning by voltage poling22 and light soaking23.

In the typical hysteresis the reverse-scan current, i.e. measured by reducing the voltage from open circuit bias (Voc) to short circuit, is larger than in the forward scan. During the reverse scan the cell behaves like a capacitor, releasing charge in the external circuit, and hence an excess of current is obtained, while during the forward scan the opposite situation occurs. We call this behavior normal hysteresis (NH). Recently an inverted hysteresis (IH) was reported in mixed-cation mixed-halide PSCs, attributed to charge extraction barriers. It was further shown that methylammonium-lead-halide PSCS with TiO2 layer covered by a thin Al2O3 insulating shell also exhibits IH. In other studies the IH was explained in terms of ionic accumulation,24 but also by the cell pre-conditioning by voltage poling and light soaking.

In this paper we report for the first time the presence of both NH and IH in the same sample, strictly depending on the applied pre-poling bias (Vpol): NH is obtained for Vpol > Voc and IH for Vpol < 0. For 0 < Vpol < Voc the hysteresis loop has a crossing point where the forward and reverse characteristics meet. The experimental data are well reproduced by the dynamic electrical model which is summarized below. Then, we indicate a three-step J-V measurement protocol which is essential for a meaningful evaluation of the hysteretic effects. We discuss the pre-poling bias conditions for the realization of NH, IH and intermediate mixed hysteresis. In connection with the measurement protocol, by controlling the switching between NH and IH, we provide further insight into PSC operation but also a systematic assessment of the dynamic hysteresis, which is crucial for a proper evaluation of the PCE.

II. THE DYNAMIC ELECTRICAL MODEL (DEM)

Several models have been considered for the dynamic hysteresis: Initially a drift-diffusion approach has been formulated, accounting for ionic migration, electronic charge traps, and recombination centers, or coupled charge carriers and defect mediated ion motion including bias scan rate and pre-poling. Then, an equivalent circuit model with constant capacitance was proposed. The DEM, recently formulated by our group, is also based on an equivalent circuit, but includes a capacitor accounting for non-linear polarization effects as depicted in Fig. II. The key assumption is that the slow process governing the time evolution of the non-linear polarization can be described by a specific relaxation time τ. Since τ is typically of the order of seconds DEM
is compatible with ion migration and accumulation at the interfaces resulting in a surface polarization of Maxwell-Wagner-Sillars type. The time dependent J-V characteristics is determined by the coupled differential equations:

\[
-R_s C_0 \frac{\partial I}{\partial t} = I_s \left( e^{\frac{q(V_{oc}+IR_s)}{nk_BT}} - 1 \right) + \left( \frac{R_s}{R_sh} + 1 \right) I + \frac{V}{R_sh} + C_0 \frac{\partial V}{\partial t} + A \frac{\partial P_{nl}}{\partial t} - I_{ph} ,
\]

(1)

\[
\frac{\partial P_{nl}}{\partial t} = P_{nl,\infty}(U_c(t)) - P_{nl}(t) \frac{\tau}{\tau},
\]

(2)

with initial conditions \( I(t = 0) = I_0 \) and \( P_{nl}(t = 0) = P_0 \), which determines the NH or IH behavior. The current density \( J \) is defined as the ratio between the current intensity \( I \) and the device active area \( A \). The elements of the circuit are: the series resistance \( R_s \), the shunt resistance \( R_{sh} \), the diode ideality factor \( n \), the diode saturation current \( I_s \), the photogenerated current \( I_{ph} \) and the geometric capacitance \( C_0 \). In contrast to the standard model with a constant capacitance, the time dependence of the non-linear polarization \( P_{nl} \) obeys Eq. (2), with a constant relaxation time \( \tau \), whereas the equilibrium polarization \( P_{nl,\infty} = (U_c/V_{oc})P_{\infty} \) depends on the voltage on the non-linear capacitor, \( U_c = V + IR_s \), where \( V \) is the external applied bias. The constant polarization \( P_{\infty} \) corresponds to \( U_c = V_{oc} \) in the steady state. The relaxation time \( \tau \) accounts for the decay of the initial polarization \( P_0 \) and also for the evolution of the polarization when the applied bias is changed. In fact, as it will be shown in the following, the current component \( I_C^{\infty} = J \times \frac{\partial P_{nl}}{\partial t} \) has a crucial role in producing the hysteretic effects, representing a significant part of the measured current \( I \):

\[
I = I_{ph} - I_d - I_{sh} - I_{c},
\]

(3)

where \( I_d \) is the diode current, \( I_{sh} \) accounts for recombinations and \( I_C = I_C^{\infty} + I_{c}^{(nl)} \), with typically negligible linear component \( I_C^{(nl)} \) due to the small geometrical capacitance \( C_0 \). However, depending on the pre-poling conditions \( I_{c}^{(nl)} \) can reach magnitudes similar to the measured current [30].

Another version of DEM has been subsequently proposed by Ravishankar et. al. [31] in terms of a relaxation kinetic constant determined by ion displacement, by reformulating Eq. (2) for the surface polarization voltage [Eq. (6) therein]. Both versions of DEM consistently reproduced experimental NH, including the dependence on the bias scan rate and the current overshoot in the reverse scan observed in several experimental studies [5, 18, 32], reproduced only in part by drift-diffusion based models [28]. The overshoot is consistent with a relaxation time of the polarization or charge accumulated at interfaces [30, 31] at the beginning of the reverse scan measurement, indicating a relation between the pre-poling bias and the initial polarization. Furthermore, the dependence of the hysteresis on the bias scan rate is consistently described by the DEM: the hysteresis is diminished at very low and very high bias scan rates, being significant at intermediate ones; importantly, the short circuit current is enhanced with the increase of the bias scan rate.

It is worth noting that a standard constant capacitance model cannot explain the current overshoot, nor can account for the diminished hysteresis at very high scan rates, unless a vanishing dielectric constant for rapidly varying fields is assumed. Moreover, it predicts only the normal hysteresis behavior.

### III. MEASUREMENT PROTOCOL

As already mentioned in other papers [32, 33], in order to obtain reproducible measurements, it is important to adopt a well defined measurement protocol. We consider three steps: 1 - the stabilization of the open circuit bias \( V_{oc} \), 2 - the solar cell pre-conditioning phase by pre-poling under 1 sun illumination, and 3 - the actual J-V measurement consisting of a single reverse-forward bias scan starting from the open circuit bias to short-circuit and back. Before each pre-conditioning phase, the solar cell is kept in open circuit under illumination until the steady state is achieved, corresponding to stabilized \( V_{oc} \) and zero current. In this way we reinitialize as far as possible the current state of the solar cell, which may be affected in successive measurements. We choose the open circuit condition for the stabilization phase, instead of the short-circuit, to avoid as much as possible the solar cell deterioration. Pre-poling with illumination is achieved by applying a constant bias \( V_{pol} \) for a time \( t_{pol} \). For \( V_{pol} > V_{oc} \) we call the sample over-polarized,
for 0 < \( V_{\text{pol}} < V_{\text{oc}} \) under-polarized, and for \( V_{\text{pol}} < 0 \) reversely polarized. Regarding the actual measurement, instead of performing individual forward and reverse bias scans, the single step reverse-forward bias scan ensures a better control over the sample pre-poling, eliminating potential pre-poling differences in the two separate scans.

**IV. RESULTS AND DISCUSSION**

*Results and discussion.* In the following we discuss the NH and IH induced by different pre-poling regimes, the measurements being consistently reproduced by the DEM calculations. The samples are prepared in the standard FTO/TiO\(_2\)/CH\(_3\)NH\(_2\)PbI\(_3-x\)Cl\(_x\)/spiro-OMeTAD/Au configuration, with \( x = 0.4 \). \[26\] as detailed in the Supporting Information (SI). More details, including the physical properties and time evolution of similar samples, are described in Ref. \[26\]. First, we calibrate the equivalent circuit elements with a measured J-V characteristics showing NH, performed at a bias scan rate of 20 mV/s, with positive pre-poling bias \( V_{\text{pol}} = 1.2 \text{V} \) for \( t_{\text{pol}} = 30 \text{s} \). With this choice, the current overshoot is present in the reverse characteristics and this marked feature enables a more accurate extraction of the model parameters \[29, 31\]. The simulated J-V characteristics of the over-polarized sample is depicted in Fig. (4a) matching closely the detailed features of the experimental data. The obtained DEM parameters are: the photogenerated current \( I_{\text{ph}} = 1.42 \text{mA} \), the series resistance \( R_s = 95 \Omega \), the shunt resistance \( R_{\text{sh}} = 3k\Omega \), the diode ideality factor \( n = 1.53 \) and saturation current \( I_s = 0.1 \text{pA} \). The relative dielectric permittivity \( \epsilon_r = 100 \) yields a quite small geometrical capacitance \( C_0 \) and its influence over the J-V characteristics is negligible in comparison with the non-linear polarization component. The steady state polarization at the open circuit is \( P_{\text{oc}} = 18 \text{mC/cm}^2 \), corresponding to a stabilized \( V_{\text{oc}} = 0.9 \text{V} \). The relaxation time \( \tau = 9 \text{s} \) fits well with the preliminary indication about the magnitude of the characteristic times involved. The assumed initial polarization \( P_0 = 9P_{\infty} \) corresponds to the pre-poling stage performed under illumination at 1.2 V for 30 s. The device active area is \( A = 0.09 \text{cm}^2 \), which is also the illuminated area.

By switching the initial polarization \( P_0 \) to negative values, J-V characteristics with mixed or completely inverted hysteresis are observed. It is quite remarkable that changing only one parameter, \( P_0 = -9P_{\infty} \), the shape of the inverted hysteresis resembles a measured characteristics with \( V_{\text{pol}} = -1\text{V} \) for 30 s at the same bias scan rate, apart from the diminished short circuit current obtained in the measurement. Taking into account \( I_{\text{ph}} = 1.11 \text{mA} \) the simulated J-V characteristics overlaps quite well with the experimental data, as indicated in Fig. (4b). Our test case shows a mostly inverted hysteresis, with a crossing point in the forward and reverse characteristics at \( \sim 0.23 \text{V} \). The decrease of \( I_{\text{sc}} \) at negative pre-poling was systematically observed in repeated measurements, starting from lower \( V_{\text{pol}} \) values to higher ones and in reverse order, which will be discussed later. Apart from this poling effect, a temporary aging of the cell is observed after repeated bias cycling, manifested by an overall decrease of the current in both forward and reverse characteristics. Typically, the samples recover in one day in dark and inert atmosphere conditions.

Both hysteretic effects can be explained by analyzing the time evolution of the non-linear polarization \( P_{i(t)} \), depicted in Fig. (5) in the case of NH, \( P_{i(t)}(t = 0) = P_0 \gg P_{\infty} \) is positive and decays rather fast in a time interval of the order of \( \tau \) in the beginning of the reverse scan. Subsequently, \( P_{\text{nl}} \) follows the bias dependent steady state polarization \( P_{\text{nl}}(t) \) [Eq. (2)] as the bias is further decreased in reverse and then increased in the forward regime. On the other hand, IH is produced by negative poling, yielding a negative initial polarization, \( P_0 < 0 \). The measurement, however, starts from \( V_{\text{oc}} \) and \( P_{\text{nl}} \) is driven into positive region on the reverse scan, reaching
To further investigate the transition between NH and IH, we measured J-V characteristics with several pre-poling voltages, between -1.5V to 1.2V, as shown in Fig. 4, together with the calculated J-V characteristics with suitably chosen initial polarizations \( P_0 \). A crossing point between the reverse and forward characteristics appears and it moves systematically towards lower biases as \( P_0 \) (or \( V_{pol} \)) decreases. This behavior was theoretically predicted before, in Ref. [30], as an under-polarization regime (\( 0 < P_0 < P_\infty \)). On the other hand, the crossing was observed experimentally [26] on aged samples with Ag counter electrodes, using a forward-reverse scan protocol starting from -0.1 V, which may be the effect of a small negative bias pre-poling, although not intentionally performed. The crossing of separately measured forward and reverse characteristics was also observed [31].

As already indicated, a particular feature is the decrease of the \( I_{sc} \) found in the measured J-V characteristics, as negative poling increases in absolute value. Based on this experimental observation and the fact that \( R_{sh} \) is relatively large, which implies \( I_{sc} \approx I_{ph} \), and assuming a relaxation time independent on the poling bias, we adjust the \( I_{ph} \) current to 1.11 mA (\( P_0 = -9P_\infty \)) and 0.96 mA (\( P_0 = -10P_\infty \)) for \( V_{pol} = -1 \) V and -1.5 V, respectively. This may be explained by iodine migration during the poling time, as negative iodine ions tend to accumulate at the TiO\(_2\) mesoporous layer and the induced electric field reduces electron collection during the subsequent measurement [25]. By contrast, when positive poling is applied the electric field induced by ions is favorable to electron extraction and \( I_{sc} \) does not change significantly.

We focus next on the bias scan rate dependence of the IH. For the NH we obtained a consistent correspondence between the measurements and DEM [30]: the NH is widest at intermediate bias scan rates and \( I_{sc} \) increases at higher rates. This behavior was explained in terms of time evolution of non-linear polarization \( P_{nl} \) and the current component \( J_{nl} = \partial P_{nl}/\partial t \) introduced in Eq. (2), as also shown (for comparison to IH) in Fig. S1 of SI. The simulated and measured J-V characteristics showing IH are presented in Fig. 5. In the experiment we considered \( V_{pol} = -1.4 \) V, which corresponds in simulations to \( P_0 = -9.5P_\infty \). At this stage the sample is slightly aged, as one may notice from the 20 mV/s scan, having

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**Figures:**

**Fig. 3.** Time evolution of the non-linear polarization \( P_{nl} \) for NH (a) and IH (b), corresponding to J-V characteristics shown in Fig. 2. The vertical arrows mark the crossing points between the bias dependent steady state polarization \( P_{nl,\infty} \) and the current polarization \( P_{nl} \). The insets show the bias dependence of \( P_{nl} \) and \( J_{nl} = \partial P_{nl}/\partial t \). The vertical dashed lines mark the separation between the reverse and forward regimes.

**Fig. 4.** Normal and inverted hysteresis, obtained by changing the pre-poling bias \( V_{pol} \) (measurements, right panel) and, correspondingly, the initial polarization \( P_0 \) (simulations, left panel), for a bias scan rate of 20 mV/s.
The NH and IH can be obtained by pre-poling the shows (SI), for an
The DEM reproduces the two hysteretic behaviors amplitude is diminished. However, the behavior of
At very fast bias scan rates there is little variation in
Our three-step protocol allows a systematic evaluation of
However in the minimal polarization case, where the
at its maximum and calculated decrease in $I_{sc}$ in IH conditions (Figs. S2 and S3). We also note that $\partial P_{nl}/\partial t < 0$ for NH and $\partial P_{nl}/\partial t > 0$ for IH, which is the reason for the crossing of the forward and reverse characteristics. We therefore conclude that the pre-poling bias is a determinant switching factor from NH to IH, which become two forms of hysteresis previously considered independent.

V. CONCLUSIONS
To conclude, we investigated the dynamic hysteresis of standard perovskite solar cells with controlled pre-conditioning. By varying the pre-poling bias, both normal and inverted hysteresis are found for the same sample and the measured J-V characteristics are closely reproduced. The main findings of the present study are:

1. The NH and IH can be obtained by pre-poling the solar cell with bias $V_{pol} > V_{oc}$ and $V_{pol} < 0$, respectively, and a mixed hysteresis is typically observed for $0 < V_{pol} < V_{oc}$.

2. The DEM reproduces the two hysteretic behaviors...
by changing only the initial polarization parameter, which is related to experimental quantities $V_{pol}$ and $t_{pol}$.

3. At higher bias scan rates the short circuit current $I_{sc}$ is enhanced for NH and lowered for IH, consistently explained by DEM.

4. The observed NH/IH behavior reveals once again the importance of controlling the solar cell pre-conditioning, particularly the bias pre-poling: the state induced by a previous measurement may inadvertently affect the next one; the designed three-step protocol, including stabilization, pre-poling and measurement is afforded for the reliability and reproducibility of the experimental data, being especially important for a correct PCE determination.

5. The presence of both NH and IH unifies apparently contradictory results reported in recent papers. Our results indicate the presence of both normal and the inverted hysteresis in the same device if the required pre-poling conditions can be achieved.

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Appendix: Supporting Information

1. Device fabrication and characterization.

a) Device fabrication

We fabricated perovskite solar cells by successive spin-coating deposition of TiO2 thin and meso-porous layers, CH$_3$NH$_3$PbI$_{3-x}$Cl$_x$ mixed halide perovskite and spiro-OMeTAD on commercial glass/FTO substrate (Solaronix TCO22-7). The compact TiO$_2$ blocking layer of 150 nm thickness is obtained from bis(acetylacetonate) solution (Aldrich) and annealing at 450 °C for 30 min. The mesoporous TiO$_2$ film (mp-TiO$_2$), composed of 20 nm size particles is deposited using a solution of TiO$_2$ commercial paste (Solaronix Ti-Nanoxide N/SP) diluted in ethanol (1:3, weight ratio). The mp-TiO$_2$ structures were first annealed at 150 °C for 5 min and then crystallized at 500 °C for 1 h. The CH$_3$NH$_3$PbI$_{3-x}$Cl$_x$ mixt halide perovskite is fabricated using the principle of one-step method [35]: a precursor solution containing 369 mg lead iodide, 56 mg lead chloride, 78 mg methyl sulfoxide, 159 mg methyl ammonium iodide (Dysol) and 600 mg dimethylformamide, homogenized for one hour, was spin coated with 2000 rpm/25 s. After 9 s from the start of the spin cycle 150 µl of diethyl ether was dripped on top of the layer, enabling the solvent extraction process to take place. The final perovskite film is obtained after annealing at 65 °C for 1 min and 100 °C for 2 min. All the above described processes were performed in normal laboratory conditions, at 24 °C and humidity between 30% and 40%. The spiro-OMeTAD was spin-coated at 1500 rpm for 30 s, in N$_2$ enriched atmosphere, at 24 °C and humidity less than 10%. The solution used for this deposition was obtained by mixing 80 mg spiro-OMeTAD (Borun Chemical), 28 µl 4-tert-butylpyridine and 18 µl of bis(trifluoromethane)sulfonimide lithium salt in acetonitrile solution (520 mg ml$^{-1}$). Gold counter electrodes of 0.09 cm$^2$ area have been deposited by magnetron RF sputtering.

b) Electrical characterization

The Photocurrent–Voltage (J–V) characteristics were measured using an Oriel VeraSol-2 Class AAA LED Solar Simulator having AM 1.5 filters and a Keithley 2400 Source Meter. The irradiation intensity was 100 mW/cm$^2$, calibrated by a Newport standard silicon solar cell 91150. The 1 Sun illumination has been performed through a rectangular aperture of 3×3 mm$^2$ size, of a geometry identical with that of Au counter electrodes.
2. Simulations and measurements revealing normal hysteresis (NH) or inverted hysteresis (IH), for different bias scan rates and prepoling biases.

a) Simulated NH and IH for different bias scan rates

FIG. S1. Simulated reverse-forward NH and IH behavior for different bias scan rates, with pre-poling $P_0 = 6P_{\infty}$ and $P_0 = -6P_{\infty}$, while all other parameters are the same as the ones used in Fig. 2(a). (a,b) J-V characteristics. (c,d) Non-linear polarization $P_{nl}$ as a function of applied bias. Time evolution of $P_{nl}$ (e,f) and $J_{c}^{(nl)}$ (g,h). At short-circuit (marked by dashed lines) $J_{c}^{(nl)}$ is increasing in absolute value with the scan rate.
b) Experimental NH and IH induced by bias pre-poling

FIG. S2. Experimental J-V characteristics showing NH and IH under pre-poling conditions: NH is obtained for positive pre-poling biases $V_{pol} = 0.6\,\text{V}, 0.8\,\text{V}, 1.0\,\text{V}, 1.2\,\text{V}$, IH is obtained for $V_{pol} = -1.5\,\text{V}$, while the mixed hysteresis characterized by a crossing point is found for $V_{pol} = -0.1\,\text{V}, -0.5\,\text{V}, -1\,\text{V}$. The poling time is in each case $t_{pol} = 30\,\text{s}$. 
c) Experimental NH and IH - influence of the bias scan rate

FIG. S3. Experimental J-V characteristics showing NH and IH for different scan rates, in the range 20 - 1000 mV/s. The samples exhibiting NH are pre-poled at $V_{pol} = 1.2\,\mathrm{V}$, while IH characteristics are obtained for $V_{pol} = -1.5\,\mathrm{V}$, with $t_{pol} = 30\,\mathrm{s}$. 
3. Influence of the waiting time at short-circuit, between reverse and forward scan, for the case of inverted hysteresis.

![Graph showing J-V characteristics for different waiting times](image)

**FIG. S4.** The influence of the waiting time $t_w$ spent at open circuit, between the reverse and forward scans (20 mV/s): simulation (a) and experiment (b). In the simulation, the relaxation time considered is $\tau = 20$ s, while the experimental pre-poling conditions are $V_{pol} = -1.5$ V and $t_{pol} = 30$ s. Other parameters which are modified for this particular sample with respect to calibration set are: $R_{sh} = 30$ k$\Omega$ and $I_{ph} = 0.6$ mA, while the initial polarization is $P_0 = -12P_\infty$. Beyond $t_w = 40$ s, the J-V characteristics tend to overlap.