Monovalent Ion Condensation at the Electrified Liquid/Liquid Interface

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X-ray reflectivity studies demonstrate the condensation of a monovalent ion at the electrified interface between electrolyte solutions of water and 1,2-dichloroethane. Predictions of the ion distributions by standard Poisson-Boltzmann (Gouy-Chapman) theory are inconsistent with these data at higher applied interfacial electric potentials. Calculations from a Poisson-Boltzmann equation that incorporates a non-monotonic ion-specific potential of mean force are in good agreement with the data.

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Interfacial ion distributions underlie numerous electrochemical and biological processes, including electron and ion transfer across charged biomembranes and energy storage in electrochemical capacitors. The solution to the Poisson-Boltzmann equation for a planar geometry, Gouy-Chapman theory, including modifications with a Stern layer, is often used to predict ion distributions near those interfaces. We showed previously that the predictions of such theories are inconsistent with x-ray reflectivity measurements of ion distributions at an electrified liquid/liquid interface. Instead, an ion-specific Poisson-Boltzmann equation (PB-PMF) that incorporated a potential of mean force (PMF) for each ion produced excellent agreement with the x-ray results. The PB-PMF theory accounts for interactions and correlations between ions and solvents that are left out of Gouy-Chapman theory. This approach has promise for understanding ion-specific effects that are relevant to many chemical processes.

Here, we demonstrate the condensation of a monovalent ion at a liquid/liquid interface. Recent theory proposes that condensation of multivalent ions is the result of strong ion-ion correlations. However, these theories do not predict such distributions for monovalent ions. Our current results can be understood by PB-PMF theory. We have chosen to fit our x-ray data to the potentials of mean force instead of fitting to a model of the electron density profile because a single PMF for each ion determines the ion distributions for all interfacial potentials.

The system under study is the liquid/liquid interface between a 100 mM aqueous solution of NaCl (Fisher Scientific) including 20 mM HEPES to buffer the pH to 7.0, and a 5 mM solution of bis(triphenyl phosphoranylidene) ammonium tetrakis(pentafluorophenyl) borate (BTPPA⁺, TPFB⁻) in 1,2-dichloroethane (DCE, Fluka). Water was produced by a Barnstead Nanopure system and DCE was purified using a column of basic alumina. BTPPATPFB was synthesized from BTPPACl (Aldrich) and LiTPFB (Boulder Scientific).

FIG. 1. Circular glass sample cell and x-ray kinematics. Electrochemical cell diagram: Ag|AgCl | 0.1M NaCl | water | +20 mM HEPES | 5 mM BTPPATPFB | DCE | 10 mM LiCl+1 mM BTPPACl | water | AgCl | Ag. A four-electrode potentiostat (Solartron 1287) is used to apply potential at counter electrodes (CE1, 2, 9 cm² Pt mesh) and monitor potential at reference electrodes (RE1, 2) in Luggin capillaries within 4 mm of interface. The liquid/liquid interface of 7 cm diameter is pinned by a Teflon strip (affixed to the glass wall) and flattened by adjusting the volume of DCE phase. Volume ratio of water:DCE is 2:1. The x-ray wave vector transfer \( \vec{Q} = \vec{k}_{out} - \vec{k}_{in} \).

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Conductance measurements using the method in Ref.\textsuperscript{8} determined that 54\% of BTPPATPFB is dissociated in DCE.

The electric potential difference $\Delta \phi^{w-o}(= \phi^{water} - \phi^{oil})$ between the water and oil (DCE) phases is given by the applied potential difference across the electrochemical cell (Fig.\textsuperscript{1}) minus the potential of zero charge ($\Delta \phi^{w-o} = \Delta \phi^{applied} - \Delta \phi^{pzc}$). We determined $\Delta \phi^{pzc} = 318 \pm 3$ mV by measuring the interfacial tension as a function of $\Delta \phi^{w-o}$\textsuperscript{2}. The ions Na$^+$ and Cl$^-$ stay primarily in the aqueous phase and BTPPA$^+$ and TPFB$^-$ stay in the DCE phase throughout the potential range studied. When $\Delta \phi^{w-o} \neq 0$, the ions form back-to-back electrical double layers at the interface. For example, when $\Delta \phi^{w-o} > 0$, the concentrations of Na$^+$ and TPFB$^-$ are enhanced at the interface while those of Cl$^-$ and BTPPA$^+$ are depleted. The variation of ionic concentration along the interfacial normal produces a variation in the electron density profile $\rho(z)$ (averaged over the x-y plane) that is probed by x-ray reflectivity.

Source\textsuperscript{2} $R(Q_z)$ is the reflected intensity normalized by the incident intensity (after subtraction of background scattering\textsuperscript{2}) as a function of wave vector transfer $Q_z = (4\pi/\lambda)\sin \alpha$, where $\lambda (=0.41255 \pm 0.00005 \, \text{Å})$ is the x-ray wavelength and $\alpha$ is the angle of incidence (Fig. 1). Figure 2 illustrates $R(Q_z)/R_F(Q_z)$ for different $\Delta \phi^{w-o}$. The variation of the peak amplitude in $R/R_F$ with increasing $\Delta \phi^{w-o}$ reveals the formation of a TPFB$^-$ layer, as discussed below.

We analyzed the x-ray data using the Poisson-Boltzmann (PB) equation,

$$\frac{d^2 \phi(z)}{dz^2} = -\frac{1}{\varepsilon \varepsilon_0} \sum_i c_i e_i^0 \exp[-\Delta E_i(z)/k_B T], \tag{1}$$

which relates the electric potential $\phi(z)$ along the interface normal $z$ to the concentration profile of ion $i$, $c_i(z) = c_i^0 \exp[-\Delta E_i(z)/k_B T]$, with Boltzmann constant $k_B$, temperature $T$, charge $e_i$ of ion $i$ (BTPPA$^+$, TPFB$^-$, Na$^+$, and Cl$^-$), permittivity of free space $\varepsilon_0$, and dielectric constant $\varepsilon$ of either DCE (10.43) for $z < 0$ or water (78.54) for $z > 0$. $\Delta E_i(z)$ is the energy of ion $i$ relative to its value in the bulk phase. The bulk ion concentration $c_i^0$ is calculated from the Nernst equation\textsuperscript{3, 12}. Fitting to the data involves calculating the electron density $\rho(z)$ and $R/R_F$ from the ion concentration profiles $c_i(z)$ as described previously\textsuperscript{2}. For the purpose of calculating $\rho(z)$ from $c_i(z)$ the ions were modeled as spheres of diameter 2Å for Na$^+$, 3.5Å for Cl$^-$, 12.6Å for BTPPA$^+$, and 10Å for TPFB$^-$, where the latter were estimated from the crystal structure of BTPPATPFB\textsuperscript{13, 14}. The TPFB$^-$ ion provides the dominant ionic contribution to the electron density profile when $\Delta \phi^{w-o} > 0$.

The Gouy-Chapman theory assumes that $E_i(z) = e_i \phi(z)$ in Eq. (1). Fits of $R/R_F$ to predictions of Gouy-Chapman theory (Fig. 2 dashed lines) used only the interfacial roughness and a $Q_z$ offset (10$^{-4}$ Å$^{-1}$, a typical misalignment of the reflectometer) as fitting parameters.
These fits agree with the data at small \( \Delta \phi^{w-o} \) (−0.12 V to 0.18 V), but at larger \( \Delta \phi^{w-o} \) (0.28 V and 0.33 V) \( R/R_F \) is greatly overestimated primarily because Gouy-Chapman theory predicts unphysically large ion concentrations near the interface.

Ion-specific effects can be included in Eq. 2 by expressing \( E_i(z) \approx e_i \phi(z) + W_i(z) \), where \( W_i(z) \) is the potential of mean force (PMF) for each ion. The PMF of Na\(^+\) was calculated from a molecular dynamics (MD) simulation for a single ion. The PMF of Cl\(^-\) was taken from an MD simulation in the literature. Fig. 3 illustrates the monotonic variation of \( W_i(z) \) for Na\(^+\) and Cl\(^-\). Due to the computational difficulties of simulating \( W_i(z) \) for large molecular ions such as BTPPA\(^+\) and TPFB\(^-\) we used a phenomenological PMF previously introduced in Ref. 2:

\[
W_i(z) = (W_i(0) - W_i^p) \frac{\text{erf}[z - \delta_i/L_i^p]}{\text{erfc}[\delta_i/L_i^p]} + W_i^p,
\]

where \( p(= w, o) \) refers to either the water phase \( (z \geq 0) \) or the oil phase \( (DCE, z \leq 0) \), \( W_i^o - W_i^w \) is the Gibbs energy of transfer of ion \( i \) from water to oil, \( \delta_i^o \) is an offset to ensure continuity of \( W_i(z) \) at \( z = 0 \), and \( L_i^o \) characterizes the decay of \( W_i(z = 0) \) to its bulk values \( W_i^w \) and \( W_i^o \). We used this monotonic PMF for BTPPA\(^+\), but had to modify it for TPFB\(^-\), as described below. Since \( W_i^o - W_i^w \) for BTPPA\(^+\) is known, the PMF of BTPPA\(^+\) is characterized by 3 parameters determined by fitting to \( R/R_F \) data at \( \Delta \phi^{w-o} = -0.12 \) V where it is expected that the BTPPA\(^+\) interfacial concentration is enhanced: \( L_i^{BTPPA^+}(= 14+12/ -6 \AA), L_i^{BTPPA^+}(= 20+11/ -6 \AA), \) and \( W_i^{BTPPA^+}(0) = 13 \pm 2 k_B T \). The large error bars on the PMF of BTPPA\(^+\) are due to the small magnitude of the most negative \( \Delta \phi^{w-o} \) that we studied.

The x-ray reflectivity at the two highest positive potentials cannot be fit if Eq. 2 is used to model the PMF for TPFB\(^-\). The simplest model that will produce the peaks in Fig. 4 is a single layer of TPFB\(^-\) ions at the interface (note that a layer of Na\(^+\), whose concentration is also enhanced at the interface, cannot provide the x-ray contrast required to fit the data). The TPFB\(^-\) layer is modeled by an attractive well in the PMF. \( W_{TPFB^-}(z) \) is given by Eq. 2 plus a Gaussian function \( D \exp[-(z - z_0)^2/2 \sigma_{PMF}^2] \) for \( z < 0 \) along with a constant offset at \( z = 0 \) to maintain continuity (see Fig. 5). Analysis with a Lorentzian produced similar results.

The six parameters of \( W_{TPFB^-}(z) \) \( [z_0, D, \sigma_{PMF}, L_i^{TPFB^-}, L_i^{TPFB^-}, W_{TPFB^-}(0)] \) along with the \( Q_z \) offset and the interfacial roughness \( (4.3 \AA < \sigma < 5.1 \AA) \) are determined by fitting \( R/R_F \) measured at \( \Delta \phi^{w-o} \) = 0.28 V and 0.33 V, where the concentration of TPFB\(^-\) is enhanced at the interface (Table I). This fitting is performed under the constraint that the resultant \( W_{ion}(z) \) produces \( R/R_F \) in agreement with the data over the entire range of potentials. In addition, fitted PMFs were rejected if the fit value of the roughness \( \sigma \) was unphysically small. In those cases an interfacial bending modulus on the order of 1000\( k_B T \) would have been required to reconcile the discrepancy of \( \sigma \) with its value predicted by capillary wave theory. In the case of the TPFB\(^-\) PMF, two local minima in \( \chi^2 \)-space (denoted \( W_{TPFB^-}(z) \) and \( W_{TPFB^-}(z) \)) were found to satisfy these conditions. Potential profiles that are intermediate between \( W_{TPFB^-}(z) \) and \( W_{TPFB^-}(z) \) do not satisfy these conditions. Most of these fits had values of \( \sigma \) within one standard deviation of capillary wave theory predictions using the measured potential-dependent interfacial tension. Fits to \( W_{TPFB^-}(z) \) at \( \Delta \phi^{w-o} = 0.28 \) V and 0.33 V had values of \( \sigma \) within two standard deviations of capillary wave theory.

The PB-PMF model with the \( W_i(z) \) shown in Fig. 3 produces \( R/R_F \) in good agreement with the data over the entire range of measured potentials (Fig. 4). The attraction

| \( W_i(z) \) \( (k_B T) \) | \( L_i^o \) \( (\AA) \) | \( L_i^w \) \( (\AA) \) | \( z_0 \) \( (\AA) \) | \( \sigma_{PMF} \) \( (\AA) \) | \( D \) \( (k_B T) \) |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| \( W_{TPFB^-}(z) \) | -5 ± 0.5         | 3 ± 0.1         | 9 ± 4           | -3.5 ± 0.2      | 3.4 ± 0.2       | -9 ± 0.25       |
| \( W_{TPFB^-}(z) \) | -25 ± 0.5        | 11 ± 0.5        | 10 ± 2.7        | -7.5 ± 0.3      | 2.6 ± 0.3       | -5.25 ± 0.2     |

FIG. 4. (left) Ion concentration profiles (in units of molarity) at \( \Delta \phi^{w-o} = 0.33 \) V calculated from PB-PMF. BTPPA\(^+\) (black), TPFB\(^-\) \[ \( W_{TPFB^-}(z)_w \); red, \( W_{TPFB^-}(z)_o \); blue \], Na\(^+\) (dots) and Cl\(^-\) (circles). (right) Electron density profiles for various potentials calculated from PB-PMF. Top to bottom: \( \Delta \phi^{w-o} = 0.33 \) V \[ \( W_{TPFB^-}(z)_w \); red, \( W_{TPFB^-}(z)_o \); blue \], 0.28V (dashed), 0.18V (solid), 0.08(dashed), -0.02V (solid), and -0.12 V (dashed).
tive wells for $W_{TPFB}^{1, II}$ have comparable depths (6 $k_B T$ for $W_{TPFB}^{I, II}$ and 5 $k_B T$ for $W_{TPFB}^{II}$), FWHM, and centers (Table 1). The ion concentration profiles $c_i(z)$ are calculated from Eq. 1 using $W_i(z)$. Figure 1 shows that the $c_i(z)$ at the highest potential, $\Delta \phi^{w-o} = 0.33 V$, take the form of two back-to-back double layers with a sharply defined layer of TPFB$^-$. The different $c_i(z)$ calculated from $W_{I, II}^{TPFB} \pm(z)$ or $W_{I}^{TPFB} \pm(z)$ differ mainly in the broadness of the profile, which in the case of $W_{I}^{TPFB} \pm(z)$ returns to its bulk value at $z = 0$, while $W_{II}^{TPFB} \pm(z)$ allows TPFB$^-$ to penetrate slightly more into the water phase. The electron density profiles $\rho(z)$ calculated from the different $c_i(z)$ are almost identical (Fig. 3), which demonstrates why our data cannot discriminate between $W_{I}^{TPFB} \pm(z)$ and $W_{II}^{TPFB} \pm(z)$.

The maximum density of TPFB$^-$ near the interface occurs at $\Delta \phi^{w-o} = 0.33 V$ and is 1 nm$^2$ per TPFB$^-$ ion when $W_{I}^{TPFB} \pm(z)$ is used or 1.5 nm$^2$ per TPFB$^-$ ion when $W_{II}^{TPFB} \pm(z)$ is used. Both values represent a high-density layer for an ion of 1 nm diameter. Although dense ionic layers have been observed in the interfacial adsorption of charged amphiphiles, the absence of a dense TPFB$^-$ layer at $\Delta \phi^{w-o} \approx 0$ indicates that TPFB$^-$ is, at most, weakly amphiphilic.

Simulations and supporting spectroscopy experiments indicate that highly polarizable ions (such as I$^-$ with a polarizability of $7.4 \AA^3$) are preferentially adsorbed to the water/vapor interface, though dense layers are not expected or observed. We calculated the polarizability of TPFB$^-$ to be $42.9 \AA^3$. This large polarizability may play a role in forming a dense layer at high potentials. Also, Borukhov et al. suggested that the entropy of the solvent can stabilize large ion adsorption. Additional theoretical work is required to determine the relevance of these two effects for the data presented here.

The MD simulations of the potentials of mean force that we used for Na$^+$ and Cl$^-$ do not account for ion-ion correlations, but they do include ion-solvent and solvent-solvent correlations. Such correlations also account for the monotonous form of $W_{BTPPA}^{+}(z)$. However, as a result of modeling the x-ray reflectivity, the phenomenological $W_{TPFB}^{-(z)}$ in Fig. 3 must implicitly account for ion-ion correlations if they are important for the observed condensation. The description of this monovalent ion condensation within PB-PMF theory illustrates the utility of this approach in describing ion-specific effects that are important for the behavior of ions in soft matter.

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