The Optical Gravitational Lensing Experiment.
Cepheids in the Magellanic Clouds.
I. Double-Mode Cepheids
in the Small Magellanic Cloud

A. Udalski¹, I. Soszyński¹, M. Szymański¹, M. Kubiaκ¹, G. Pietrzyński¹, P. Woźniak², and K. Żebruń¹

¹Warsaw University Observatory, Al. Ujazdowskie 4, 00-478 Warszawa, Poland
e-mail: (udalski,soszynski,msz,mk,pietrzyn,zebrun)@sirius.astrouw.edu.pl
²Princeton University Observatory, Princeton, NJ 08544-1001, USA
e-mail: wozniak@astro.princeton.edu

ABSTRACT

We present a sample of 93 double-mode Cepheids detected in the 2.4 square degree area in the central part of the SMC, 23 stars from the sample pulsate in the fundamental mode and the first overtone while 70 objects are the first and second overtone pulsators. This is the largest sample of such type Cepheids detected in one environment so far.

We analyze period ratio of double-mode Cepheids and Fourier parameters of decomposition of the light curves of these objects. We also present location of different type Cepheids from the SMC in the color-magnitude diagram and show their distribution of $V-I$ color indices. We find one object which is probably a blend, either physical or optical, of two Cepheids pulsating in the fundamental mode.

1 Introduction

Microlensing searches for dark matter in the Galaxy provide an unique by-product – huge databases of precise photometric measurements of tens million stars in the Magellanic Clouds and dense Galactic fields. The measurements span a few years and are ideally suited for variable star study. One of the group of variable stars profiting a lot from microlensing surveys data

*Based on observations obtained with the 1.3 m Warsaw telescope at the Las Campanas Observatory of the Carnegie Institution of Washington.
are pulsating variable stars. The Magellanic Clouds offer an ideal sample of those stars due to their large population there and approximately the same distance. Unfortunately, they have been neglected photometrically for years.

About 1400 Cepheids were identified in the Large Magellanic Cloud by the MACHO microlensing team (Alcock et al. 1995). The majority of objects are regular single-mode pulsators. Alcock et al. (1995) also presented a sample of 45 double-mode Cepheids identified among detected objects. The double-mode Cepheids (called sometimes beat Cepheids) pulsate simultaneously in two radial modes: either fundamental and first overtone (FU/FO) or first and second overtones (FO/SO). The double-mode Cepheids are relatively rare, only fourteen were identified in the Galaxy so far (Pardo and Poretti 1997). Large sample of double-mode Cepheids from the LMC, increased later to 75 objects, allowed for more detailed study of properties of these objects (Alcock et al. 1999).

The double-mode Cepheids were also identified in the Small Magellanic Cloud. 27 object sample was reported by the MACHO team (Alcock et al. 1997) and 11 object sample by the EROS team (Beaulieu et al. 1997). The sample of the SMC Cepheids is very important because smaller metallicity of the SMC allows to study dependence of pulsation properties of double-mode Cepheids on their metallicity.

The Magellanic Clouds were included to the observing targets of the Optical Gravitational Lensing Experiment (OGLE) microlensing search at the beginning of the second phase of the project, OGLE-II, in January 1997 (Udalski, Kubiak and Szymański 1997). After two years of constant monitoring of the Magellanic Clouds, the photometric databases of the OGLE project are complete enough to allow for search for Cepheids in the Magellanic Clouds. In this paper, first of the series on Cepheid variable stars in the Magellanic Clouds, we present results of the search for double-mode Cepheids in the central regions of the SMC leading to discovery of 93 such objects – the largest sample of double-mode Cepheids detected so far.

2 Observations

All observations presented in this paper were carried out during the second phase of the OGLE experiment with the 1.3-m Warsaw telescope at the Las Campanas Observatory, Chile, which is operated by the Carnegie Institution of Washington. The telescope was equipped with the "first generation"
camera with a SITe 2048 × 2048 CCD detector working in the drift-scan mode. The pixel size was 24 µm giving the 0.417 arcsec/pixel scale. Observations of the SMC were performed in the "slow" reading mode of the CCD detector with the gain 3.8 e−/ADU and readout noise about 5.4 e−. Details of the instrumentation setup can be found in Udalski, Kubiak and Szymański (1997).

Observations of the SMC started on June 26, 1997. As the microlensing search is planned to last for a few years, observations of selected fields will be continued during the following seasons. In this paper we present data collected up to March 4, 1998. Observations were obtained in the standard $BVI$-bands with majority of measurements made in the $I$-band.

Photometric data collected during the first observing season of the SMC for 11 fields (SMC_SC1–SMC_SC11) covered about 2.4 square degree of the central parts of the SMC and were used to construct the $BVI$ photometric maps of the SMC (Udalski et al. 1998a). The reader is referred to that paper for more details about methods of data reduction, tests on quality of photometric data, astrometry, location of observed fields etc.

3 Selection of Double-Mode Cepheids

The search for variable objects in 11 SMC fields was performed using observations in the $I$-band in which majority of observations was obtained. Typically about 160–200 epochs were available for each analyzed object with the lower limit set to 50. The mean $I$-band magnitude of objects was limited to $I < 20$ mag. Candidates for variable stars were selected based on comparison of the standard deviation of all individual measurements of a star with typical standard deviation for stars of similar brightness. Light curves of selected candidates were then searched for periodicity using the AoV algorithm (Schwarzenberg-Czerny 1989).

Candidates for Cepheids were selected from the entire sample of variable stars based on visual inspection of the light curves and location in the color-magnitude diagram (CMD) within the area limited by $I<18.5$ mag and $0.25<(V-I)<1.3$ mag. Several objects located outside this region but with evident Cepheid light curves were also included to this sample (e.g., highly reddened Cepheids). In total more than 2300 Cepheid candidates were found in the 2.4 square degree area of the SMC bar. The catalog of all objects will be presented in the following papers of this series.

Selection of double-mode Cepheids was performed in two stages. First,
in the preliminary search, we used results of the general variable star search described above. The mean light curve folded with the AoV period of each Cepheid candidate was fitted by high order polynomial and subtracted from the light curve. Double-mode Cepheids usually fold with the higher amplitude periodicity displaying abnormally large scatter in the light curve. The residuals were then searched for periodic signal and, if detected, such a candidate was marked for further analysis. Then a histogram of the ratio of the shorter to the longer period of selected double-mode Cepheid candidates was constructed. It exhibited two clear sharp peaks corresponding to the ratio of the first overtone to the fundamental period, ≈ 0.735, and the second to the first overtone period, ≈ 0.805, in good agreement with Alcock et al. (1997). The list of the double-mode Cepheid candidates from this search included stars having the period ratio within ±0.02 from these values – the range wide enough to avoid missing potential outliers.

The second, final search for double-mode Cepheids was performed using the CLEAN algorithm of period determination (Roberts, Lehár and Dreher 1987). All 2300 objects from the Cepheid candidate list were subjected to the CLEAN period analysis. Having well established limits for the period ratio of double-mode Cepheids from the preliminary analysis, only those objects which exhibited suitable period ratio (±0.015) between the highest peak in the power spectrum and one of the next four strongest peaks were further analyzed. The final list of the double-mode Cepheid candidates presented in this paper was obtained after careful visual inspection of the CLEAN power spectra of each object.

4 Double-Mode Cepheids in the SMC

Double-mode Cepheids detected in the central area of the SMC are listed in Tables 1 and 2. 95 objects were detected but 93 of them are unique. Two stars are located in the overlapping regions between fields and they were discovered independently in each field. Table 1 contains systems which pulsate in the fundamental and first overtone modes while Table 2 – objects pulsating in the first and second overtones. Basic parameters of each star: right ascension and declination (J2000), the intensity-mean $I$-band magnitude, $(B - V)$ and $(V - I)$ colors, both periods and their ratio are provided. Accuracy of periods is about $7 \cdot 10^{-5} P$. Finding charts for all objects are presented in Appendix A. The size of the $I$-band subframes is $60 \times 60$ arcsec; North is up and East to the left.
### Table 1
FU/FO Double-Mode Cepheids in the SMC

| Field  | Star No. | RA(J2000) | DEC(J2000) | $P_{FO}$ | $R_{21}^{FO}$ | $\phi_{21}^{FO}$ | $P_{FU}$ | $R_{21}^{FU}$ | $\phi_{21}^{FU}$ | $P_{FO}/P_{FU}$ | $I$ | $R-V$ | $V-I$ | Remarks |
|--------|----------|-----------|------------|----------|----------------|-----------------|----------|----------------|-----------------|----------------|-----|-------|-------|---------|
| SMC/SC1 | 35550 | 0°37′32″012 -73°30′33″1 | 1.054 | 0.206 | 4.356 | 2.546 | 1.431 | 0.000 | - | - | 0.736 | 17.095 | 0.404 | 0.589 |
| SMC/SC2 | 60587 | 0°36′31″23 -73°39′20″4 | 0.814 | 0.255 | 3.915 | 1.504 | 1.104 | 0.091 | 3.274 | - | - | 0.737 | 17.246 | 0.458 | 0.582 |
| SMC/SC3 | 61760 | 0°41′58″84 -73°23′00″5 | 1.310 | 0.231 | 4.866 | 2.575 | 1.790 | 0.190 | 4.429 | - | - | 0.734 | 16.638 | 0.413 | 0.660 |
| SMC/SC4 | 56827 | 0°44′40″49 -73°24′39″2 | 1.297 | 0.165 | 4.646 | - | 1.777 | 0.140 | 4.051 | - | - | 0.730 | 16.927 | 0.511 | 0.703 |
| SMC/SC5 | 75443 | 0°46′12″62 -72°46′56″4 | 1.581 | 0.178 | 5.078 | 2.154 | 0.109 | 4.334 | - | - | 0.729 | 16.207 | 0.529 | 0.621 |
| SMC/SC6 | 145181 | 0°47′38″51 -72°42′45″3 | 1.268 | 0.208 | 4.204 | 0.748 | 1.713 | 0.187 | 4.741 | - | - | 0.740 | 15.379 | 0.411 | 0.504 |
| SMC/SC7 | 175210 | 0°48′21″56 -73°07′17″3 | 1.340 | 0.240 | 4.725 | 3.306 | 1.840 | 0.227 | 4.442 | - | - | 0.733 | 16.080 | 0.387 | 0.649 |
| SMC/SC8 | 117506 | 0°49′33″33 -73°06′32″9 | 1.668 | 0.147 | 4.873 | 3.724 | 2.097 | 0.139 | 4.410 | - | - | 0.735 | 17.180 | 0.068 | 0.975 |
| SMC/SC9 | 155033 | 0°49′54″21 -72°40′54″0 | 1.636 | 0.118 | 5.237 | 4.697 | 2.432 | 0.172 | 4.855 | - | - | 0.729 | 16.439 | 0.507 | 0.698 |
| SMC/SC10 | 219903 | 0°50′44″08 -72°53′36″7 | 1.633 | 0.150 | 5.168 | 3.823 | 2.231 | 0.213 | 4.505 | 2.506 | 0.731 | 16.501 | 0.513 | 0.750 |
| SMC/SC11 | 49926 | 0°52′10″85 -72°55′28″5 | 1.457 | 0.220 | 4.906 | 3.111 | 2.021 | 0.168 | 4.380 | - | - | 0.729 | 16.514 | 0.357 | 0.702 |
| SMC/SC12 | 77317 | 0°51′57″98 -72°40′39″0 | 1.221 | 0.170 | 4.828 | 3.024 | 1.662 | 0.140 | 3.766 | - | - | 0.734 | 16.749 | 0.608 | 0.671 |
| SMC/SC13 | 221538 | 0°53′13″99 -72°52′42″6 | 1.587 | 0.174 | 5.083 | 3.197 | 2.180 | 0.158 | 4.548 | - | - | 0.728 | 16.358 | 0.498 | 0.663 |
| SMC/SC14 | 57228 | 0°55′11″47 -72°38′19″0 | 1.402 | 0.253 | 4.794 | 3.466 | 1.911 | 0.184 | 4.464 | 2.944 | 0.733 | 16.589 | 0.488 | 0.670 |
| SMC/SC15 | 70881 | 0°56′53″25 -72°27′08″8 | 1.343 | 0.191 | 4.630 | 3.362 | 1.834 | 0.153 | 4.591 | - | - | 0.732 | 16.149 | 0.427 | 0.576 |
| SMC/SC16 | 164739 | 0°56′18″44 -73°03′46″7 | 1.284 | 0.190 | 4.448 | 2.970 | 1.754 | 0.000 | - | - | 0.732 | 16.769 | 0.424 | 0.597 |
| SMC/SC17 | 197655 | 0°56′15″62 -72°34′52″5 | 1.502 | 0.189 | 4.824 | - | 2.054 | 0.153 | 4.476 | - | - | 0.733 | 16.525 | 0.482 | 0.645 |
| SMC/SC18 | 249966 | 0°57′19″80 -72°35′11″9 | 0.643 | 0.140 | 3.676 | - | 0.863 | 0.000 | - | - | 0.745 | 17.753 | 0.520 | 0.706 |
| SMC/SC19 | 30899 | 0°58′06″52 -72°27′11″1 | 1.372 | 0.253 | 5.493 | 3.302 | 1.877 | 0.140 | 3.537 | - | - | 0.733 | 17.461 | 0.556 | 0.618 |
| SMC/SC20 | 105810 | 1°00′18″63 -72°30′04″7 | 1.610 | 0.171 | 5.039 | - | 2.221 | 0.093 | 3.888 | - | - | 0.729 | 16.190 | 0.478 | 0.661 |
| SMC/SC21 | 128768 | 1°06′35″71 -72°24′42″2 | 1.670 | 0.223 | 4.965 | 2.925 | 2.285 | 0.204 | 4.531 | - | - | 0.730 | 16.198 | 0.505 | 0.698 |
| SMC/SC22 | 24037 | 1°06′41″71 -72°24′42″9 | 1.670 | 0.214 | 4.990 | 3.502 | 2.286 | 0.191 | 4.620 | - | - | 0.730 | 16.210 | 0.494 | 0.695 |

Remarks: M: Double-mode Cepheid reported by MACHO (Acock et al. 1997); U: uncertain; S: same star as SMC_SC10 128768
### Table 2

FO/SO Double-Mode Cepheids in the SMC

| Field | Star No. | RA (J2000) | DEC (J2000) | $P_{SO}$ | $R_{21}^{SO}$ | $\phi_{21}^{SO}$ | $P_{FO}$ | $R_{21}^{FO}$ | $\phi_{21}^{FO}$ | $P_{SO}/P_{FO}$ | $I$ | $B-V$ | $V-I$ | Remarks |
|-------|----------|------------|-------------|---------|--------------|----------------|---------|--------------|----------------|---------------|-----|-------|-------|---------|
| SMC C1 | 20157 | 0°36'51''24 | -73°14'42''4 | 0.68762 | 0.130 | 5.375 | 0.85458 | 0.300 | 4.093 | 0.80463 | 16.950 | 0.332 | 0.529 | M |
| SMC C2 | 14736 | 0°39'25''04 | -73°13'00''6 | 0.54069 | 0.000 | – | 0.67043 | 0.239 | 4.005 | 0.80648 | 17.194 | 0.319 | 0.503 | |
| SMC C2 | 19900 | 0°39'33''70 | -73°01'27''0 | 0.54438 | 0.124 | 4.877 | 0.67490 | 0.256 | 3.948 | 0.80661 | 17.249 | 0.235 | 0.569 | M |
| SMC C2 | 31653 | 0°40'34''96 | -73°30'03''9 | 0.57816 | 0.000 | – | 0.71748 | 0.314 | 3.819 | 0.80582 | 17.298 | 0.376 | 0.534 | |
| SMC C2 | 46929 | 0°40'27''29 | -72°59'51''0 | 0.54367 | 0.161 | 5.585 | 0.67460 | 0.250 | 3.636 | 0.80591 | 17.442 | 0.407 | 0.595 | |
| SMC C2 | 97203 | 0°42'13''29 | -73°13'09''9 | 0.67717 | 0.112 | 4.190 | 0.84264 | 0.275 | 4.102 | 0.80363 | 17.233 | 0.422 | 0.641 | M |
| SMC C3 | 20000 | 0°42'56''00 | -73°18'25''1 | 0.56937 | 0.185 | 2.793 | 0.70585 | 0.283 | 3.948 | 0.80686 | 17.458 | 0.358 | 0.579 | M |
| SMC C3 | 35943 | 0°43'08''17 | -73°03'46''9 | 0.54626 | 0.257 | 4.475 | 0.67706 | 0.197 | 3.638 | 0.80681 | 17.595 | 0.420 | 0.590 | M |
| SMC C3 | 115945 | 0°44'29''18 | -73°33'42''8 | 0.63146 | 0.244 | 1.151 | 0.78528 | 0.276 | 3.878 | 0.80412 | 17.293 | 0.354 | 0.528 | U |
| SMC C4 | 2356 | 0°45'03''39 | -73°31'08''5 | 0.55999 | 0.399 | 3.116 | 0.69077 | 0.218 | 3.760 | 0.80633 | 17.295 | 0.367 | 0.508 | |
| SMC C4 | 8429 | 0°45'49''47 | -73°23'45''0 | 0.52784 | 0.000 | – | 0.65506 | 0.191 | 3.537 | 0.80579 | 17.276 | 0.316 | 0.518 | |
| SMC C4 | 82181 | 0°46'46''74 | -72°58'32''4 | 0.50404 | 0.129 | 4.993 | 0.62485 | 0.233 | 3.680 | 0.80666 | 17.423 | 0.386 | 0.521 | |
| SMC C4 | 101024 | 0°47'20''96 | -73°31'26''3 | 0.66873 | 0.174 | 5.128 | 0.83097 | 0.306 | 4.010 | 0.80476 | 17.045 | 0.387 | 0.554 | M |
| SMC C4 | 106956 | 0°47'08''11 | -73°23'54''8 | 0.59592 | 0.000 | – | 0.73921 | 0.324 | 3.989 | 0.80616 | 16.867 | 0.378 | 0.559 | M |
| SMC C4 | 106992 | 0°47'37''88 | -73°22'42''4 | 1.03622 | 0.140 | 5.233 | 1.31230 | 0.153 | 3.756 | 0.80486 | 16.639 | 0.544 | 0.724 | |
| SMC C4 | 110510 | 0°47'15''10 | -73°20'19''2 | 0.49322 | 0.000 | – | 0.61132 | 0.237 | 3.644 | 0.80681 | 17.568 | 0.486 | 0.574 | U |
| SMC C4 | 131229 | 0°47'10''49 | -72°58'44''0 | 0.80409 | 0.241 | 5.499 | 1.00823 | 0.185 | 4.164 | 0.80182 | 17.006 | 0.525 | 0.668 | |
| SMC C4 | 150011 | 0°48'00''07 | -73°31'54''5 | 0.49172 | 0.168 | 4.639 | 0.60983 | 0.281 | 3.602 | 0.80632 | 17.363 | 0.332 | 0.491 | M |
| SMC C4 | 150163 | 0°47'38''87 | -73°30'06''9 | 0.52885 | 0.000 | – | 0.65650 | 0.255 | 3.634 | 0.80556 | 17.539 | 0.335 | 0.574 | |
| SMC C4 | 153342 | 0°48'10''79 | -73°27'56''6 | 0.57542 | 0.232 | 3.596 | 0.71429 | 0.314 | 3.883 | 0.80558 | 17.355 | 0.452 | 0.645 | |
| SMC C4 | 163672 | 0°48'32''10 | -73°18'02''1 | 0.46360 | 0.000 | – | 0.57435 | 0.130 | 3.036 | 0.80717 | 17.705 | 0.432 | 0.625 | U |
| SMC C4 | 171521 | 0°48'05''44 | -73°09'54''5 | 0.54163 | 0.182 | 4.569 | 0.67212 | 0.266 | 3.619 | 0.80585 | 17.586 | 0.278 | 0.824 | |
| SMC C4 | 182628 | 0°48'03''42 | -73°00'06''8 | 0.77097 | 0.000 | – | 0.95956 | 0.245 | 4.023 | 0.80346 | 16.813 | 0.430 | 0.605 | |
| SMC C4 | 186443 | 0°48'22''25 | -72°55'10''3 | 0.62631 | 0.000 | – | 0.77443 | 0.232 | 3.253 | 0.80874 | 16.827 | 0.654 | 0.874 | |
Table 2
Continued

| Field | Star No | RA(J2000) | DEC(J2000) | \( P_{SO} \) | \( R_{SO} \) | \( \phi_{SO} \) | \( P_{FO} \) | \( R_{FO} \) | \( \phi_{FO} \) | \( P_{SO}/P_{FO} \) | \( B-V \) | \( V-I \) | Remarks |
|-------|---------|-----------|------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|---------|
| SMC.SC5 | 16449 | 05:48:49.92 | -73°19'45"3 | 0.56769 | 0.154 | 5.339 | 0.70421 | 0.184 | 3.934 | 0.80614 | 17.307 | 0.396 | 0.584 |
| SMC.SC5 | 70168 | 05:48:59.17 | -72°44'01"2 | 0.53037 | 0.168 | 5.234 | 0.65810 | 0.236 | 3.636 | 0.80391 | 17.346 | - | 0.510 | M |
| SMC.SC5 | 129596 | 05:49:27"36 | -72°59'36"6 | 0.60638 | 0.175 | 5.034 | 0.75250 | 0.267 | 3.837 | 0.80582 | 17.389 | 0.424 | 0.619 |
| SMC.SC5 | 170398 | 05:50:02"33 | -73°23'09"1 | 0.67750 | 0.127 | 4.252 | 0.84209 | 0.234 | 4.034 | 0.80455 | 16.817 | 0.448 | 0.579 |
| SMC.SC5 | 230217 | 05:50:43"97 | -72°44'42"4 | 0.89780 | 0.089 | 1.756 | 1.11558 | 0.215 | 4.027 | 0.80476 | 16.487 | 0.417 | 0.605 |
| SMC.SC5 | 235535 | 05:50:46"60 | -72°40'56"0 | 0.60191 | 0.122 | 4.920 | 0.74684 | 0.312 | 3.762 | 0.80594 | 17.061 | 0.329 | 0.497 |
| SMC.SC5 | 240099 | 05:51:21"55 | -73°35'48"6 | 0.51894 | 0.154 | 6.043 | 0.64238 | 0.250 | 3.421 | 0.80784 | 17.588 | 0.409 | 0.623 |
| SMC.SC5 | 266081 | 05:51:13'77 | -73°14'03"7 | 0.70446 | 0.000 | - | 0.87304 | 0.172 | 3.808 | 0.80690 | 16.986 | 0.511 | 0.651 |
| SMC.SC5 | 289174 | 05:55:55"83 | -73°00'13"5 | 0.58283 | 0.000 | - | 0.72293 | 0.178 | 4.176 | 0.80621 | 17.618 | 0.480 | 0.714 |
| SMC.SC5 | 294824 | 05:52:09"94 | -72°58'04"1 | 0.59290 | 0.117 | 4.132 | 0.73505 | 0.189 | 3.932 | 0.80661 | 17.124 | 0.410 | 0.610 |
| SMC.SC5 | 306011 | 05:50:09"90 | -72°31'00"9 | 0.66677 | 0.182 | 4.616 | 0.82864 | 0.282 | 4.116 | 0.80466 | 17.253 | 0.507 | 0.693 |
| SMC.SC5 | 306021 | 05:51:16"95 | -72°56'41"5 | 0.61124 | 0.000 | - | 0.75929 | 0.270 | 3.873 | 0.80502 | 17.086 | 0.386 | 0.577 |
| SMC.SC6 | 17580 | 05:52:10"34 | -73°13'19"8 | 0.61781 | 0.138 | 3.783 | 0.76693 | 0.243 | 3.791 | 0.80556 | 17.316 | 0.382 | 0.614 |
| SMC.SC6 | 129043 | 05:52:55"42 | -72°59'18"4 | 0.57559 | 0.174 | 2.933 | 0.71391 | 0.247 | 4.019 | 0.80625 | 17.297 | 0.381 | 0.521 | M |
| SMC.SC6 | 158249 | 05:53:33"94 | -72°42'50"5 | 0.58160 | 0.191 | 5.903 | 0.72200 | 0.271 | 4.036 | 0.80554 | 17.322 | 0.412 | 0.564 |
| SMC.SC6 | 180332 | 05:53:08"57 | -73°20'48"6 | 0.49649 | 0.271 | 4.936 | 0.6415 | 0.208 | 3.003 | 0.80842 | 17.455 | 0.386 | 0.582 |
| SMC.SC6 | 190505 | 05:53:14"61 | -73°12'53"6 | 0.58669 | 0.278 | 4.001 | 0.72834 | 0.207 | 3.877 | 0.80552 | 17.417 | 0.397 | 0.643 | M |
| SMC.SC6 | 195101 | 05:53:39"36 | -73°09'20"8 | 0.57939 | 0.235 | 3.695 | 0.71930 | 0.264 | 3.904 | 0.80549 | 17.219 | 0.353 | 0.506 |
| SMC.SC6 | 246813 | 05:53:22"73 | -72°35'21"3 | 0.59226 | 0.186 | 5.867 | 0.73479 | 0.198 | 3.997 | 0.80603 | 17.150 | 0.145 | 0.699 |
| SMC.SC6 | 251147 | 05:53:15"56 | -72°31'31"9 | 0.58204 | 0.000 | - | 0.72411 | 0.283 | 3.973 | 0.80569 | 17.235 | 0.316 | 0.581 |
| SMC.SC6 | 277080 | 05:54:04"94 | -73°05'51"1 | 0.87847 | 0.146 | 4.739 | 1.09587 | 0.199 | 4.110 | 0.80162 | 16.610 | 0.363 | 0.627 |
| SMC.SC6 | 291809 | 05:54:08"59 | -72°56'33"8 | 0.59053 | 0.244 | 4.268 | 0.63070 | 0.225 | 3.621 | 0.80629 | 17.362 | 0.326 | 0.514 |
| SMC.SC7 | 4204 | 05:54:49"93 | -73°15'00"6 | 0.50949 | 0.151 | 6.019 | 0.73323 | 0.230 | 3.871 | 0.80533 | 17.182 | 0.479 | 0.525 |
| SMC.SC7 | 8786 | 05:55:03"01 | -73°15'50"0 | 0.66904 | 0.195 | 3.887 | 0.83081 | 0.218 | 4.031 | 0.80529 | 17.136 | 0.341 | 0.562 |
| Field | Star No. | RA(J2000) | DEC(J2000) | $P_{SO}$ [days] | $R_{SO}^{21}$ | $\phi_{SO}^{21}$ | $P_{PO}$ [days] | $R_{PO}^{21}$ | $\phi_{PO}^{21}$ | $P_{SO}/P_{PO}$ | I [mag] | B - V [mag] | V - I [mag] | Remarks |
|-------|----------|-----------|------------|----------------|-------------|--------------|----------------|-------------|--------------|----------------|---------|-------------|-------------|---------|
| SMC.SC7 | 42358 | 0°54′59″19 | −72°34′15″2 | 0.68167 | 0.348 | 4.576 | 0.84817 | 0.281 | 3.938 | 0.80370 | 17.169 | 0.450 | 0.598 |         |
| SMC.SC7 | 100561 | 0°55′36″76 | −73°00′33″8 | 0.68260 | 0.234 | 5.493 | 0.84935 | 0.265 | 4.054 | 0.80367 | 16.897 | 0.454 | 0.620 |         |
| SMC.SC7 | 133650 | 0°55′54″58 | −72°32′30″7 | 0.62520 | 0.000 | − | 0.77637 | 0.287 | 3.881 | 0.80529 | 17.291 | 0.386 | 0.600 |         |
| SMC.SC8 | 137641 | 0°55′30″22 | −72°31′18″7 | 0.52324 | 0.161 | 4.203 | 0.64867 | 0.300 | 3.731 | 0.80664 | 17.228 | 0.391 | 0.484 |         |
| SMC.SC8 | 30693 | 0°57′57″62 | −72°38′08″3 | 0.57695 | 0.000 | − | 0.71541 | 0.246 | 3.699 | 0.80646 | 17.490 | 0.531 | 0.634 | M         |
| SMC.SC8 | 52895 | 0°57′47″19 | −72°18′03″5 | 0.68079 | 0.210 | 0.065 | 0.84470 | 0.214 | 3.376 | 0.80595 | 16.792 | 0.375 | 0.579 |         |
| SMC.SC8 | 62881 | 0°58′49″63 | −73°00′52″3 | 0.66639 | 0.126 | 4.419 | 0.82868 | 0.254 | 4.045 | 0.80416 | 17.286 | 0.477 | 0.604 |         |
| SMC.SC8 | 66186 | 0°58′21″52 | −75°58′50″5 | 0.64056 | 0.000 | − | 0.79688 | 0.299 | 3.952 | 0.80383 | 17.230 | 0.360 | 0.585 | U         |
| SMC.SC8 | 94906 | 0°58′50″10 | −72°31′41″3 | 0.71048 | 0.126 | 4.934 | 0.85413 | 0.283 | 4.040 | 0.80359 | 17.321 | 0.456 | 0.705 |         |
| SMC.SC8 | 113418 | 0°58′59″34 | −73°05′00″3 | 0.45432 | 0.000 | − | 0.56318 | 0.262 | 3.511 | 0.80670 | 17.694 | 0.331 | 0.524 |         |
| SMC.SC8 | 122864 | 0°59′11″91 | −75°55′18″3 | 0.56490 | 0.165 | 4.601 | 0.70033 | 0.215 | 3.670 | 0.80662 | 17.337 | 0.490 | 0.559 | M         |
| SMC.SC8 | 139476 | 0°59′13″40 | −73°38′42″4 | 0.70065 | 0.000 | − | 0.87091 | 0.268 | 3.918 | 0.80450 | 16.834 | 0.280 | 0.567 |         |
| SMC.SC8 | 186707 | 0°59′58″15 | −74°42′14″7 | 0.56577 | 0.120 | 4.302 | 0.70203 | 0.295 | 3.710 | 0.80591 | 17.507 | 0.386 | 0.658 |         |
| SMC.SC9 | 21140 | 1°00′59″27 | −72°37′18″6 | 0.56594 | 0.000 | − | 0.62729 | 0.245 | 3.791 | 0.80655 | 17.548 | 0.352 | 0.509 |         |
| SMC.SC9 | 47742 | 1°00′56″53 | −72°04′43″1 | 0.46623 | 0.000 | − | 0.57668 | 0.278 | 3.557 | 0.80847 | 17.463 | − | 0.542 |         |
| SMC.SC9 | 99981 | 1°02′19″78 | −72°51′48″1 | 0.43307 | 0.189 | 3.742 | 0.61126 | 0.261 | 3.776 | 0.80665 | 17.508 | 0.391 | 0.483 | M         |
| SMC.SC9 | 108504 | 1°02′07″98 | −73°39′49″0 | 0.49770 | 0.000 | − | 0.61713 | 0.258 | 3.604 | 0.80648 | 17.413 | 0.357 | 0.538 |         |
| SMC.SC10 | 52945 | 1°05′08″51 | −72°40′04″3 | 0.54366 | 0.000 | − | 0.67485 | 0.253 | 3.747 | 0.80560 | 17.253 | 0.303 | 0.543 | U         |
| SMC.SC10 | 124662 | 1°05′50″28 | −72°29′34″9 | 0.87666 | 0.000 | − | 0.72949 | 0.264 | 4.004 | 0.80558 | 17.136 | 0.366 | 0.569 |         |
| SMC.SC10 | 128831 | 1°06′17″31 | −72°22′01″6 | 0.59299 | 0.184 | 4.832 | 0.73599 | 0.252 | 3.896 | 0.80570 | 17.271 | 0.434 | 0.614 |         |
| SMC.SC11 | 13365 | 1°06′34″76 | −72°41′04″4 | 0.51491 | 0.277 | 4.191 | 0.63875 | 0.169 | 3.750 | 0.80612 | 17.236 | 0.358 | 0.493 |         |
| SMC.SC11 | 24118 | 1°06′17″30 | −72°22′01″7 | 0.59286 | 0.274 | 4.679 | 0.73597 | 0.234 | 3.919 | 0.80555 | 17.286 | 0.438 | 0.597 | S         |
| SMC.SC11 | 42383 | 1°07′37″33 | −72°45′50″6 | 0.64988 | 0.117 | 3.905 | 0.80714 | 0.270 | 3.700 | 0.80516 | 17.128 | 0.353 | 0.575 |         |

**Remarks:** M: Double-mode Cepheid reported by MACHO (Alcock et al. 1997); U: uncertain; S: same star as SMC.SC10 128831
Appendices B and C show the light curves of FU/FO and FO/SO pulsators, respectively. The first and second columns in each Appendix contain original photometric data folded with the shorter and longer periods while the remaining columns show variability attributed to each mode after subtraction of the other period variability approximated by Fourier series of fifth order. For objects revealing also periodicity equal to the sum and/or difference of both mode frequencies and having an amplitude larger than twice the formal error – such terms were also subtracted from the original data. BVI photometry of all objects will be available from the OGLE Internet archive when the catalog of Cepheids in the SMC is released.

Completeness of the sample is determined by completeness of the variable star search in the OGLE databases and efficiency of double-mode Cepheid detection algorithm. Completeness of the OGLE variable stars catalog was already estimated for eclipsing stars which are much more difficult to detect. For objects brighter than $I = 17$ it is likely to be higher than 90% (Udalski et al. 1998b). For stars as bright and easy to detect as Cepheids it should be similar or even higher. Completeness of the detection algorithm can be assessed by comparison of results obtained in the preliminary and final (CLEAN) searches. More than 90% objects in both lists are common suggesting good completeness of the search.

As a test of completeness we cross-identified double mode Cepheids reported by MACHO (Alcock et al. 1997). 19 out of 20 objects which are located in the OGLE fields were detected during our search. They are marked by letter ‘M’ in the last column of Tables 1 and 2. The remaining object, MACHO*00:57:27.0-73:04:39, was also analyzed but it seems to be a single period Cepheid.

5 Discussion

93 double-mode Cepheids were identified during the presented search in the 2.4 square degree area in the central bar of the SMC. 23 objects pulsate simultaneously in the fundamental mode and first overtone while 70 objects in the first and second overtones. The sample constitutes the most numerous sample of double-mode Cepheids located in one environment. Completeness of the sample is high, likely larger than 90%.
5.1 Period Ratio in Double-Mode Cepheids

Fig. 1 presents the ratio of periods of the FU/FO and FO/SO pulsators plotted as a function of the lower mode period. In both cases a clear dependence on the period is seen, similarly to the Galactic and LMC Cepheids (Alcock et al. 1995). More numerous sample allows for more precise approximation of that dependence.

![Graph showing the ratio of periods in double-mode Cepheids plotted as a function of the longer period. Dotted and solid lines mark the best linear fits given by Eqs. 1 and 2, respectively.]

The best linear fits are as follows:

**FU/FO Cepheids:**

\[ P_{\text{FO}} / P_{\text{FU}} = 0.741 - 0.032 \times \log P_{\text{FU}}, \]

\[ 0.001 \quad 0.005 \]  

**FO/SO Cepheids:**

\[ P_{\text{SO}} / P_{\text{FO}} = 0.804 - 0.014 \times \log P_{\text{FO}}. \]

\[ 0.001 \quad 0.002 \]

Comparison of coefficients in Eqs. (1) and (2) with similar ones for the Galactic and LMC double-mode Cepheids:

\[ P_{\text{FO}} / P_{\text{FU}} = 0.733 - 0.034 \times \log P_{\text{FU}} \]
\[
\frac{P_{SO}}{P_{FO}} = 0.803 - 0.022 \times \log P_{FO}
\]
for the LMC Cepheids and
\[
\frac{P_{FO}}{P_{FU}} = 0.720 - 0.027 \times \log P_{FU}
\]
for the Galactic Cepheids (Alcock et al. 1995) indicates that the ratio of periods for FU/FO pulsators is slightly larger for the SMC Cepheids than for the LMC and Galactic objects which are more metal rich: \([\text{Fe}/\text{H}] = -0.7\) for the SMC Cepheids vs. \([\text{Fe}/\text{H}] = -0.3\) and \([\text{Fe}/\text{H}] = 0.0\) for the LMC and Galactic Cepheids, respectively. On the other hand the ratio for FO/SO Cepheids is almost identical with the ratio of the LMC objects but the slope of the relation is flatter.

### 5.2 Fourier Decomposition of Light Curves of Double-Mode Cepheids

Fourier decomposition of light curves of pulsating stars has been widely used for analyzing their properties (Simon and Lee 1981). In the case of Cepheids the ratio of amplitudes of the first harmonic and the fundamental period, \(R_{21} = A_2/A_1\), and phase difference, \(\phi_{21} = \phi_2 - 2\phi_1\) are particularly useful. Both allow to distinguish between the fundamental mode and first overtone pulsators. The \(R_{21}\) vs. \(\log P\) diagram constructed for about 1400 Cepheids from the LMC (Alcock et al. 1999) shows two distinct and well separated "V-shape" sequences for Cepheids pulsating in the fundamental mode and the first overtone. In the similar diagram \(\phi_{21}\) vs. \(\log P\) the sequences for both modes of pulsation are also well defined but the separation is smaller and in some ranges of periods they overlap.

Fig. 2 presents the \(R_{21}\) vs. \(\log P\) and \(\phi_{21}\) vs. \(\log P\) diagrams constructed for about 2300 single-mode Cepheids (small dots) from the SMC. The Cepheids come from the preliminary catalog of Cepheids in the SMC, and therefore some very tiny contamination by non-Cepheid variable stars is still possible in these diagrams. Nevertheless both diagrams look basically the same as for the LMC Cepheids with well-separated "V-shape" sequences in the \(R_{21}\) vs. \(\log P\) diagram and two characteristic sequences in the \(\phi_{21}\) vs. \(\log P\) diagram.

To check behavior of double-mode Cepheids we decomposed their light curves to the sum of two Fourier series of fifth order corresponding to both periodicities including the terms of sum and difference of mode frequencies when their amplitudes were larger than twice the formal errors. Then we
Fig. 2. $R_{21}$ and $\phi_{21}$ vs. log $P$ diagrams for single-mode Cepheids from the SMC (small dots). Large open and filled circles mark values of the first overtone and fundamental mode pulsations in the FU/FO double-mode Cepheids, respectively. Star symbols denote values of $R_{21}$ and $\phi_{21}$ for "double Cepheid", SMC SC5 208044.
calculated $R_{21}$ and $\phi_{21}$ for both pulsating modes. They are listed in Tables 1 and 2.

Results for the FU/FO Cepheids are shown in Fig. 2: the values for the fundamental mode pulsation are plotted with large filled dots while for the first overtone mode with open circles. Objects with non-significant first harmonic amplitude, $A_2$, \(i.e.,\) with almost sinusoidal light curve) have $R_{21} = 0$ and their $\phi_{21}$ is not defined.

The main conclusion which can be drawn from Fig. 2 is that while the first overtone pulsations usually dominate in this class of double-mode Cepheids and their $R_{21}$ and $\phi_{21}$ fall in the sequences of the single-mode first overtone pulsators, the fundamental mode pulsations have $R_{21}$ values much smaller than corresponding single-mode fundamental mode Cepheids. This means that the fundamental mode pulsations in double-mode Cepheids are suppressed making the light curve not that sharp and more sinusoidal than for single-mode Cepheids of that type. In the most extreme cases the funda-
mental mode pulsations are low amplitude almost sinusoidal variations (see Appendix B).

$\phi_{21}$ values of the fundamental mode pulsations in double-mode Cepheids seem to fall largely in the fundamental mode Cepheid sequence. Unfortunately, in this part of the $\phi_{21}$ vs. log $P$ diagram the sequences of the fundamental mode and first overtone Cepheids overlap. Therefore the diagram is not fully conclusive.

Mantegazza and Poretti (1992) suggested that the phase difference of the second harmonic and fundamental period, $\phi_{31} = \phi_3 - 3\phi_1$ might be better for discrimination between the first overtone and fundamental mode pulsating objects. The sequences for the first overtone and fundamental mode Cepheids are better separated in the $\phi_{31}$ vs. log $P$ than in the $\phi_{21}$ vs. log $P$ diagram. Therefore we constructed the $\phi_{31}$ vs. log $P$ diagram for all single-mode Cepheids with statistically significant second harmonic amplitude. The diagram is plotted in Fig. 3. Small dots represent single-mode Cepheids.

Indeed, two well separated sequences starting from approximately (log $P = 0, \phi_{31} = 2$) are clearly seen. The steeper one is populated by stars pulsating in the first overtone while the second one, more horizontal but rising rapidly at (log $P = 0.9, \phi_{31} = 4$) and better populated, by fundamental mode pulsators. The $\phi_{31}$ values are periodic with the period equal to $2\pi$ and they are shown in Fig. 3 in the range $0 - 2\pi$. Therefore two additional sequences starting at (log $P = 0.5, \phi_{31} = 0$) and (log $P = 1.0, \phi_{31} = 0$) are simply continuation of the first overtone and fundamental mode Cepheid sequences, respectively.

We calculated the $\phi_{31}$ values for all double-mode Cepheids of FU/FO type with statistically significant second harmonic amplitude. The values are listed in Table 1. Open circles in Fig. 3 mark positions of the first overtone pulsation values. As can be seen they fall well in the single-mode first overtone Cepheid sequence similar to the previous diagrams. Unfortunately, for the fundamental mode pulsations the $\phi_{31}$ values could only be derived for two objects from the sample, SMC_SC5 219993 and SMC_SC7 57228 because the second harmonic amplitude is non-significant for the remaining Cepheids. $\phi_{31}$ of these stars are plotted with filled dots in Fig. 3. Both values are located in the sequence of single-mode Cepheids pulsating in the fundamental mode. We may, thus, conclude that the longer period pulsations in the FU/FO double-mode Cepheids are indeed of the fundamental mode type in spite of the fact that their $R_{21}$ is smaller as compared to the values of single-mode objects in the $R_{21}$ vs. log $P$ diagram.
Fig. 4. $R_{21}$ and $\phi_{21}$ vs. log $P$ diagrams for single-mode Cepheids from the SMC (small dots). Large open and filled circles mark values of the second and first overtone pulsations in the FO/SO double-mode Cepheids, respectively.
Fig. 4 presents $R_{21}$ vs. $\log P$ and $\phi_{21}$ vs. $\log P$ diagrams for FO/SO double-mode Cepheids from the SMC. The first overtone pulsation values of $R_{21}$ and $\phi_{21}$ are plotted with large filled dots while those calculated for the second overtone pulsations with open circles.

The first overtone pulsations also dominate in this group of objects. Their $R_{21}$ and $\phi_{21}$ values are located exactly in the corresponding sequences of the single-mode first overtone Cepheids. The second overtone pulsations are typically low amplitude quasi sinusoidal light variations (see Appendix C). For many objects the first harmonic amplitude, $A_2$, of the second overtone period is not statistically significant ($i.e., R_{21} = 0$), while for the remaining ones it is usually very small making $R_{21}$ small, typically below 0.2. The $\phi_{21}$ values for the second overtone pulsations are usually larger than those corresponding to the first overtone sequence providing another way of distinguishing between those two modes of pulsations.

5.3 SMC Cepheids in the Color-Magnitude Diagram

Huge and homogeneous sample of Cepheids from the observed region of the SMC located practically at the same distance and relatively small extinction toward the SMC make it possible to analyze in detail location of different types of Cepheids in the color-magnitude diagram and their distribution of color indices, that is the temperature distribution of different mode pulsators.

We selected four classes of Cepheids: single-mode fundamental and first overtone pulsators and double-mode FU/FO and FO/SO objects. The single-mode stars were divided into the first overtone and fundamental mode groups based on location in the $R_{21}$ vs. $\log P$ and period-luminosity ($\langle I \rangle$ vs. $\log P$) diagrams. These samples included 705 and 1148 objects, respectively.

For all objects the intensity-mean magnitudes in the $V$ and $I$-bands were calculated. Then the magnitudes of objects from fields SMC\_SC2–SMC\_SC11 were corrected for difference of the mean reddening between the field in which a given object is located and the mean reddening in the SMC\_SC1 field. The mean difference of reddening between SMC\_SC1 and the remaining fields was derived based on the mean difference of the $I$-band magnitudes of the red clump stars in corresponding fields. The mean $I$-band magnitude of the red clump stars is a good reference of brightness (Udalski 1998a,b), particularly in homogeneous environment like central parts of the SMC. Similar method was used to determine map of extinction of the Baade’s Window in the Galactic bulge by Stanek (1996).
Fig. 5. Color-magnitude diagram of the SMC_SC1 field. Only about 20% of field stars are plotted by tiny dots. Larger dots show positions of single-mode fundamental type Cepheids (darker dots) and first overtone stars (lighter dots). Large filled circles and star symbols mark positions of the FU/FO and FO/SO double-mode Cepheids, respectively.
Thus, magnitudes of all Cepheids were tied to the reference field SMC_SC1. The mean extinction of the latter field is $A_I = 0.11$ mag, corresponding to $E(B-V) = 0.06$ and $E(V-I) = 0.08$, based on the mean $I$-band magnitude of the red clump stars, $I = 18.457$, and the mean extinction free magnitude of the red clump stars in the SMC (Udalski 1998a,b).

Fig. 5 presents the CMD of the field SMC_SC1. Only about 20% of field stars were plotted by tiny dots for clarity. Single-mode Cepheids are plotted with larger dots: fundamental mode – darker dots, first overtone – lighter dots. Positions of FU/FO double-mode Cepheids are indicated by large filled circles while FO/SO objects by star symbols.

Fig. 5 is a detailed picture of location of the instability strip in the SMC. The blue edges of the instability strip for both – fundamental and first-overtone Cepheids are very well defined. The strip goes almost vertically up to $I \approx 15$ and bends toward red for brighter objects – mostly fundamental mode Cepheids. The red edge is somewhat less sharp because of several objects reddened more than the mean reddening correction applied to each field. Nevertheless it can also be precisely determined.

Double-mode Cepheids are clumped in two distinct locations. The FU/FO pulsators are on average by about 0.8 mag brighter than FO/SO objects. They form a vertical sequence in the part of the instability strip populated by both kinds of single-mode Cepheids: from the blue part of the instability strip of fundamental mode Cepheids and the red part of the strip of first overtone objects. The FO/SO pulsators populate largely low luminosity blue part of the strip of single-mode first overtone Cepheids. They also form a vertical sequence about 1 mag long defining the region where such kind pulsations are possible.

### 5.4 Colors of Double-Mode Cepheids

More quantitative information on differences of four groups of Cepheids in the SMC can be obtained by analyzing the distribution of color indices (i.e., temperature distribution).

Fig. 6 shows histograms of $(V-I)$ color indices of all four groups of Cepheids. The width of the bin is 0.03 mag. Thick solid and dotted lines correspond to the single-mode fundamental and first overtone Cepheids while thin solid and dotted lines to the FU/FO and FO/SO double-mode pulsators. All histograms were fitted with a Gaussian which fits well the observed color distributions. In the case of single-mode fundamental mode Cepheids there is a small excess of red objects caused by the redward bending of the insta-
bility strip for the brightest stars. When we limit our sample to the objects fainter than $I = 15$ mag, the excess disappears.

The mean $V - I$ color and the standard deviation of its distribution are 0.673, 0.08 (0.666, 0.08 for $I > 15$ sub-sample) and 0.573, 0.08 for the single-mode fundamental and first overtone Cepheids, respectively. For FU/FO and FO/FO double-mode Cepheids the corresponding values are: 0.634, 0.05 and 0.545, 0.05, respectively. The single-mode first overtone Cepheids are on average by about 0.1 mag bluer than fundamental mode pulsators. As one could expect the FU/FO double-mode Cepheids have $V - I$ color distribution in between the first and fundamental mode distributions of single-mode stars. The color distribution of FO/FO double-mode Cepheids resembles that of the single-mode first overtone stars but it is
shifted bluewards.

5.5 "Double Cepheid" in the SMC

The final search with the CLEAN algorithm was aimed at detection of double-mode Cepheids by constraining the searched periods to the range around the period ratio of double-mode Cepheids. This approach omits, however, potential objects which are a Cepheid blended with another periodic object. For instance, three such cases of "double Cepheids" in the LMC were reported by Alcock et al. (1995). To look for similar objects in the SMC we reran our searching procedure with another constraint, namely only stars with the second peak in the power spectrum (third if the second peak was the harmonic of the most prominent one, etc), with frequency outside the double-mode Cepheid range and higher than one fourth of the first peak power were selected.

![Fig. 7. Light curve of "double Cepheid", SMC_SC5 208044. The upper panels show the original data folded with two detected periods while the lower panels the light curve of each component after subtraction of variability of the second star approximated by Fourier series of fifth order.](image)

One object from this sample, SMC_SC5 208044 (RA(J2000) = 0\textdegree 50\text{"}38\text{.}78, DEC(J2000) = -72\textdegree 59\text{"}02\text{.}1"), seems to consist of two blended Cepheids. Fig. 7 shows the light curves of both components of the blend. The finding chart is shown in Fig. 8.

Both components seem to be fundamental mode pulsators and although
their period ratio, 0.715, is close to the FU/FO double-mode Cepheid range, the shape of the light curves of both components and Fourier parameters marked in Fig. 2 by star symbols leave little doubts that they are two distinct, blended objects. Such an interpretation is also supported by larger brightness of the star than other objects of similar period and also lack of periodicity corresponding to the sum and difference of two detected frequencies which in a double-mode Cepheid of such a large amplitude should be easily detectable. It is impossible to conclude whether the system is only an optical blend or components are physically bounded. Spectroscopic observations could provide additional information to clear this problem.

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