Observation of polarised hard X-ray emission from the Crab by the PoGOLite Pathfinder

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ABSTRACT
We have measured the linear polarisation of hard X-ray emission from the Crab in a previously unexplored energy interval, 20–120 keV. The introduction of two new observational parameters, the polarisation fraction and angle stands to disentangle geometrical and physical effects, thereby providing information on the pulsar wind geometry and magnetic field environment. Measurements are conducted using the PoGOLite Pathfinder - a balloon-borne polarimeter. Polarisation is determined by measuring the azimuthal Compton scattering angle of incident X-rays in an array of plastic scintillators housed in an anticoincidence well. The polarimetric response has been characterised prior to flight using both polarised and unpolarised calibration sources. We address possible systematic effects through observations of a background field. The measured polarisation fraction for the integrated Crab light-curve is (18.4±9.8)% corresponding to an upper limit (99% credibility) of 42.4%, for a polarisation angle of (149.2±16.0)°.

Key words: instrumentation: polarimeters – techniques: polarimetric – X-rays: Crab

1 INTRODUCTION

At radio, optical and infrared wavelengths, polarimetry has become an established probe of source radiation mechanisms and geometry. The application to X-ray sources has not evolved as rapidly since relatively long exposures of sensitive, purpose-built instruments are needed. The positive definite nature of measurements presents a significant challenge for instrument design and characterisation. Measurements of linear X-ray polarisation provide two additional observation parameters, the polarisation fraction (%) and polarisation angle (photon electric vector orientation). The addition of these parameters stands to elucidate emission processes and geometry in sources containing ordered magnetic fields, e.g. pulsars, or high degrees of asymmetry, e.g. accretion disks and columns (e.g. Lei et al. 1997; Krawczynski et al. 2011).

The scientific potential of X-ray polarisation studies is recognised by the plethora of proposed missions¹. Eventually, satellite-based polarimeters are expected to provide defining studies of a large number of sources, e.g.

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¹ For a recent survey, see http://ttt.astro.su.se/groups/head/cost14/
XIPE (Soffitta et al. 2013) (ESA Medium Class mission), IXPE (Weisskopf et al. 2008) and PRAXYS (NASA Small Explorer missions) were recently selected for further study. Despite comparatively short observation times and the effect of residual atmosphere, polarisation measurements using purpose-built instruments operating from stratospheric ballooning platforms (altitude $\sim 40$ km) can provide initial data-sets and opportunities for methodology development. In this paper, we report polarisation results from such a balloon mission - the PoGOLite Pathfinder (Chauvin et al. 2015a), which is a purpose-designed Compton polarimeter with sensitivity in the energy range 20–240 keV. The polarimetric response has been characterised prior to flight with both polarised and unpolarised beams (Chauvin et al. 2016).

As one of the brightest sources on the sky, the Crab pulsar and wind nebula system is a natural first light candidate for PoGOLite. Although perhaps the most studied extrasolar celestial object (Hester 2008), details of the high energy emission, including fundamental questions such as location, remain unresolved. The emission site may (a) take place in open field line regions close to the neutron star surface above the polar cap, as seen for radio pulses (Harding et al. 1995; Daugherty et al. 1996); (b) occur in the outer magnetosphere along the last open field line between the null-charge surface and the light cylinder (Romani 1996; Cheng 2000); (c) or concern an intermediate region (Dyks et al. 2004), along the edge of the open field region extending from the surface of the neutron star out to the light cylinder. The models predict high degrees of linear polarisation with significant variations across the pulsar phase. This mirrors the behaviour seen in optical measurements (Slowikowska et al. 2009) due to a common dependence on field line geometry. Precision spectral studies of the Crab by Fermi (Abdo et al. 2010) favour high energy emission in the outer magnetosphere. The emission is almost certainly synchrotron in nature, but curvature radiation has also been proposed by Sturrock et al. (1975). An observation of the spectral properties of the emission is not sufficient to distinguish between these two processes. Polarisation measurements provide discrimination since the polarisation vector in synchrotron emission is perpendicular to the magnetic field line direction while there is a parallel arrangement for curvature radiation. Furthermore, Satori et al. (1967) have proposed a two temperature plasma model describing Crab emissions through bremsstrahlung processes. In this case, the emission is predicted to be unpolarised.

Novick et al. (1972) reported the first detection of X-ray polarisation (5–20 keV) for the Crab nebula with a sounding rocket payload. A highly significant measurement was subsequently provided by an instrument on-board the OSO-8 satellite mission (Weisskopf et al. 1976) during a 256 ks observation. A high polarisation fraction was reported, e.g. (19.2±1.0)% at 2.6 keV, compatible with expectations for synchrotron processes, as expected from earlier spectral studies at radio and optical wavelengths. The measured polarisation angle of $(156.4\pm0.1)^{\circ}$ is displaced from the direction of the pulsar spin axis projected onto the sky, $(124.0\pm0.1)^{\circ}$, inferred from the torus inclination (Ng et al. 2004). More recently, the IBIS (Förot et al. 2008) and SPI (Dean et al. 2008) instruments on-board the INTEGRAL satellite have measured the polarisation of Crab emissions for selected pulsar phase windows. Unlike OSO-8, these instruments were not designed for polarimetry nor calibrated as such prior to launch.

2 METHOD

We perform observations using PoGOLite, a Compton polarimeter. The Klein Nishina differential Compton scattering cross-section dictates that X-rays are more likely to scatter in the direction perpendicular to the polarisation vector. The resulting sinusoidal distribution, $f(\phi)$, of azimuthal scattering angles, $\phi$, is referred to as a modulation curve and carries information about the polarisation fraction and angle. The modulation curve has the form

$$f(\phi) = N(1 + A \cos(2(\phi - \phi_0))),$$

where $A$ is the peak-to-peak amplitude of the modulation, $N$ is the number of events and $\phi_0$ is the phase of the modulation, related to the polarisation angle, $\psi = \phi_0 - 90^{\circ}$.

Azimuthal scattering angles are measured in a close-packed array of 20 cm long and 3 cm wide (center-to-center) hexagonal plastic scintillator rods. Two-hit polarisation events are characterised by a Compton scatter in one rod followed by a second Compton scatter or a photoelectric absorption in another rod. The entire detector volume is rotated around the viewing axis once every 300 s in order to mitigate instrument systematics such as variations in efficiency between detector elements. Aperture background is reduced with an active collimator system which defines the field-of-view of the polarimeter to $2.4^{\circ} \times 2.6^{\circ}$. The plastic scintillator target is housed within a segmented active BGO (Bi$_4$Ge$_3$O$_{12}$) anticoincidence well, surrounded by a thick polyethylene neutron shield.

Assuming an unpolarised background during observations, the modulation factor is defined as

$$M = A \times (1 + 1/R),$$

where $R$ is the signal-to-background ratio. The reconstructed polarisation fraction is defined as $p = M/M_{100}$, where $M_{100}$ is the modulation factor for a 100% polarised incident beam with defined spectral properties. When performing a $\chi^2$ fit to a histogram of scattering angles the statistical uncertainty on $p$ is derived by standard error propagation as

$$\sigma_p^2 = \frac{1}{M_{100}^2} \left[ \left( 1 + \frac{1}{R} \right)^2 \times \sigma_A^2 + \frac{A^2}{R^2} \times \sigma_R^2 + \frac{A^2 \times \left( 1 + \frac{1}{R} \right)^2}{M_{100}^2} \times \sigma_{100}^2 \right],$$

where $\sigma_A$, $\sigma_R$ and $\sigma_{100}$ are the statistical uncertainties on $A$, $R$ and $M_{100}$, respectively. The statistical uncertainty on the polarisation angle is simply $\sigma_{\psi} = \sigma_{\phi_0}$, as derived from the $\chi^2$ fit.

An alternative method for computing $p$ uses the Stokes parameters. Following the formalism in Kislat et al. (2015), $Q$ and $U$ are defined as

$$Q = \frac{1}{N_S} \sum_{i=1}^{N} \cos 2\psi_i, \quad U = \frac{1}{N_S} \sum_{i=1}^{N} \sin 2\psi_i,$$

where $N_S$ is the total number of signal events. This method
has the advantage that it is not affected by subjectivity when choosing the binning of the modulation curve. However, the absence of goodness-of-fit information, which can reveal distortions of the modulation curve, may yield spurious polarisation results. The polarisation fraction and angle are given by

\[ p = \frac{2}{M_{100}} \sqrt{Q^2 + U^2}, \quad \psi = \frac{1}{2} \arctan \frac{U}{Q}. \]  

(5)

The statistical uncertainties on these quantities are

\[ \sigma_p \approx \sqrt{\frac{2 - p^2 M_{100}^2}{(N - 1) M_{100}^2}}, \quad \sigma_\psi \approx \frac{1}{p M_{100} \sqrt{2(N - 1)}}, \]  

(6)

not taking into account the statistical uncertainty on \( R \) and \( M_{100} \).

A figure-of-merit often used for describing the sensitivity of a polarimeter is the Minimum Detectable Polarisation, MDP (Weisskopf et al. 2010), where

\[ \text{MDP} = \frac{4.29 \sqrt{N}}{M_{100} N_S} \]  

(7)

at 99% confidence level. If a measurement yields a polarisation fraction equal to the MDP, there is a 1% probability that the measured value arises from a statistical fluctuation of an unpolarised flux. A measurement of polarisation is possible when the reconstructed polarisation fraction lies below the MDP but the uncertainties on such a measurement are non-Gaussian leading to a biased polarisation fraction, i.e. \( \Pi \neq \psi \), where \( \Pi \) is the true polarisation fraction. Although \( \Psi = \psi \), where \( \Psi \) is the true polarisation angle, \( \sigma_\Phi \neq \sigma_\psi \) (\( \sigma_\Phi \) is the uncertainty on the true polarisation angle) because the uncertainty given by equation 6 or by a \( \chi^2 \) fit to the modulation curve is assumed to be Gaussian but \( \Psi \) is not Gaussian distributed. We have therefore developed a Bayesian method (Mikhailov et al. 2015) based on Maier et al. (2014) for converting \( p \) to \( \Pi \) and computing the two dimensional credibility regions for \( \Pi \) and \( \Psi \). The likelihood is sampled using a Monte Carlo approach and inverted using the integral form of Bayes’ theorem. This allows the posterior distribution of \( (\Pi, \Psi) \) to be determined for a measured polarisation \( p \). This Bayesian approach requires a prior, which, considering the discussion in Quinn (2012), is chosen to be uniform in polar coordinates \( (\Pi, \Psi) \) and limited to \( 0 < \Pi < 1 \).

3 OBSERVATIONS AND DATA REDUCTION

The PoGOLite Pathfinder was launched from the Esrange Space Centre in Northern Sweden on July 12th 2013 on a near circumpolar flight (Chauvin et al. 2015a). The polarimeter is suspended \( \sim 100 \) m under a helium filled \( 10^6 \) m\(^3\) balloon. An attitude control system aligns the polarimeter optical axis to sources with a precision exceeding \( 0.01^\circ \) in RA and Dec. We observed the Crab during each of the first three days of the flight for a total of 32.9 ks. Observing conditions are summarised in Table 1. We only consider observations with column density \( < 0.8 \) g cm\(^{-2}\) to avoid degrading the MDP. A total of 122 993 two-hit polarisation events are considered for analysis for the energy range 20–120 keV, which is dictated by the polarimeter effective area for Crab observations and atmospheric attenuation. The average energy of measured photons is 46 keV. The procedure described in (Chauvin et al. 2016) was followed to compute the Crab \( M_{100} \) for the flight event selection criteria described in (Chauvin et al. 2015a), yielding (21.4 \( \pm \) 1.5)%.

We used data\(^2\) from the HXD instrument (Takahashi et al. 2007) on the Suzaku satellite (10–70 keV energy range) to produce a reference light-curve. The difference in energy range between PoGOLite and HXD has negligible impact on the reference light-curve (Kokubun et al. 2007). We compared the measured and reference light-curves to determine \( R = 0.252 \pm 0.026 \) which results in MDP = \( (28.4 \pm 2.2)\% \).

Polarisation fraction is a positive definite quantity. It is therefore important to show that observations of background fields yield a modulation curve which is statistically consistent with an unpolarised signal. Prior to flight, we planned observations of background fields displaced 5\(^\circ\) in RA and Dec from the Crab. Problems with the thermal control of the polarimeter during observations prevented this approach. Instead, we conducted background studies in the anti-Sun direction with the polarimeter directed at Cygnus X-1, which was originally unforeseen as a secondary observation target. However, the prevailing soft spectral state and average column density during background observations of 6.5 g cm\(^{-2}\) (5.7 g cm\(^{-2}\) for Crab observations) resulted in an estimated two-hit \( R \) of 1:27 for the PoGOLite energy range, based on fluxes measured by Swift BAT (Krimm et al. 2013). This results in a negligible signal count rate.

4 ANALYSIS AND RESULTS

4.1 Background observations

As described in Chauvin et al. (2016), anisotropic background may result in a modulation of the scattering angle, which cannot be removed by the rotation of the polarimeter around its optical axis. To show that atmospheric background does not induce a false modulation signature, we use background observations (9 ks) with a similar elevation range as Crab observations. Each scattering angle is transformed to the Crab frame of reference by applying a field rotation correction in the range

\[ \text{Table 1. Summary of Crab observations.} \]

| Date       | Observation time (ks) | Altitude (km) | Column density (g cm\(^{-2}\)) | Two-hit events |
|------------|-----------------------|--------------|-------------------------------|----------------|
| July 12th  | 2.6                   | 38.6–39.9    | 5.9–6.8                       | 11 154         |
| July 13th  | 19.1                  | 38.3–39.9    | 4.6–6.8                       | 70 700         |
| July 14th  | 11.2                  | 38.2–39.0    | 5.7–6.8                       | 41 139         |

\(^2\) Public data-set 104001070.
included the amplitude is more significant, the Stokes method avoids binning subjectivity and yields statistical consistency when obtaining the true polarisation fraction, \( \Pi \), and angle, \( \Psi \), from the reconstructed polarisation fraction, \( p \), and angle, \( \psi \), in the Stokes analysis. As described in Mikhalev et al. (2015), this approach also accounts for the uncertainty on the measurement of \( R \) due to the fitting of the reference light-curve and the uncertainty on \( M_{100} \) due to limited calibration statistics. The resulting probability distribution contour plot is shown in Figure 3.

Figure 4 is obtained by marginalising the contour plot over the polarisation angle (i.e. projecting onto the polarisation fraction axis). The peak corresponds to the most likely (highest posterior density) true polarisation \( \Pi = (18.4^{+9.8}_{-10.6})\% \) where the asymmetric uncertainty represents the tightest credibility region (not the statistical uncertainty on the peak) enclosing 68.3\% (one Gaussian standard deviation) probability content. The upper limit, at 99\% credibility, is 42.4\%. Marginalising over the polarisation fraction gives Figure 5. The polarisation angle is \( \Psi = (149.2 \pm 16.0)^{\circ} \), measured relative to North in an anticlockwise direction (i.e. to the East). The posterior distribution for the background contribution derived from background observations is also shown in Figure 4. The corresponding point-estimate for the polarisation fraction is 0\%. The 99\% upper limit on the background contribution is 11.2\%.

### 5 DISCUSSION

In this paper, we present the first measurement of the linear polarisation of Crab emissions in the 20-120 keV energy interval. We have used a purpose-built polarimeter which has been calibrated with both polarised and unpolarised beams prior to launch, as required due to the positive definite nature of the measurements. Through the use of background field observations, we have addressed the response of the polarimeter to potentially anisotropic background, and show that this does not induce a statistically significant polarisation signal. We present results integrated over the entire

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**Table 2.** Polarisation parameters as derived from \( \chi^2 \) fitting and Stokes method. Here \( A \), \( p \) and \( \psi \) are the modulation amplitude, polarisation fraction and polarisation angle, respectively.

| Bkgd  | \( \chi^2 \) | \( A \) \( \pm \) \( 0.49 \pm 0.83 \)% | \( p \) | \( \psi \) |
|-------|-------------|---------------------------------|------|------|
| Stokes| \( (0.49 \pm 0.83)\% \) | - | - | - |

Since \( p < MDP \), a Bayesian approach is required to properly account for statistical uncertainties and to determine credibility regions when obtaining the true polarisation fraction, \( \Pi \), and angle, \( \Psi \), from the reconstructed polarisation fraction, \( p \), and angle, \( \psi \), in the Stokes analysis.

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**Figure 1.** The modulation curve for background observations.

**Figure 2.** The modulation curve for Crab observations.

**Figure 3.** The posterior distribution of the polarisation fraction and angle from PoGOLite Crab observations. The magenta lines are contours corresponding to 1, 2 and 3 standard deviation Gaussian probability content. The color bar is the probability per bin.
In the optical regime, this alignment suggests that polarised hard X-ray emission originates close to the pulsar. Possible emission sites have been identified through a detailed study at optical wavelengths by Moran et al. (2013) which shows that the polarisation of wisps, the inner knot and torus are well aligned to the pulsar spin axis and have \( \sim 50\% \) polarisation fraction.

A second high latitude long duration balloon flight will be conducted in July 2016. Based on experience from the 2013 flight, we will improve the polarimeter design with particular focus on improving the \( M_{100} \) and background reduction methods (Chauvin et al. 2015b). This will allow the contribution from the nebula to be isolated through pulse phase selections.

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