Tropical cyclone forecast using NCMRWF Global (12 km) and regional (4 km) models

RAGHAVENDRA ASHRT, SUSHANT KUMAR, ANUMEHA DUBE, T. ARULALAN, S. KARUNASAGAR, A. ROUTRAY, SAJI MOHANDAS, JOHN. P. GEORGE and A. K. MITRA

National Centre for Medium Range Weather Forecasting, Ministry of Earth Sciences, A-50, Institutional Area, Phase-2, Sec-62, Noida (U.P.) – 201 309, India

e mail : raghu@ncmrwf.gov.in

ABSTRACT. Countries adjoining the North Indian Ocean (NIO) region are among the world’s worst affected areas by tropical cyclones (TCs). An increase in frequency and intensity of TCs affecting this basin is noticed in recent years. Timely and accurate prediction of a TC can lead to a decrease in damages to life and property caused by the cyclone. In recent times, the forecasts of TC tracks and intensity have improved due to advancements in the resolution, data assimilation techniques and physics of Numerical Weather Prediction (NWP) models and improvements in the model’s initial condition. In this study, we have analysed the forecasts of Super Cyclone (SuCS) ‘Amphan’ that occurred over the Bay of Bengal during 16-21 May, 2020 obtained from the Global and Regional version of the NCMRWF Unified Model, i.e., NCUM-G and NCUM-R, respectively.

The analysis of the track error shows that the initial position and 24-hour forecast errors in both the models are very close. However, the 48 to 72-hour forecast errors are much lower in the NCUM-R compared to NCUM-G. The percentage decrease in the track errors from global to regional model is about 12% in the 48-hour forecasts and 17% in the 72-hour forecasts. The landfall position error is less than 50 km in the predictions after 18 May, 2020 in NCUM-G. However, NCUM-R shows a lower landfall location error as compared to NCUM-G. Comparing the intensity forecasts from NCUM-G and NCUM-R shows that the 48 hrs forecast of minimum sea level pressure (SLP) based on initial conditions of 16th May, 2020 are very close to the observed intensity. The rapid intensification of Amphan is also well predicted by both the models, although with a delay. The cyclone structure shows that the 850 hPa vorticity core is much stronger in NCUM-R forecasts than NCUM-G. The warm-core system in the NCUM-R forecasts is also more organized than in NCUM-G. On the other hand, the maximum wind radius is greater in NCUM-G forecasts than NCUM-R.

Key words – Cyclone track errors, Landfall location error, Intensity verification, Rapid intensification, Regional models.
1. Introduction

The North Indian Ocean (NIO) is affected by tropical cyclones (TCs) in two seasons, namely, the pre-monsoon season, which lasts from March to May and the post-monsoon season which lasts from October to December (Mohanty et al., 2010). The intensity and frequency of cyclones have seen an increase over the NIO basin in recent years (Singh et al., 2000; Balaji et al., 2018). There were a total of 19 cyclones starting from 2018 to November 2020. Out of these cyclones, eight were intensified to the level of Severe Cyclonic Storms, 3 were Extremely Severe Cyclones and two were in the category of Super cyclonic storms. It can be seen that the number of intense cyclones is increasing in the NIO region and resulting in very significant damage to life and property. This damage can be minimized by a timely and accurate prediction of the cyclone's location and intensity.

In recent years, there has been a remarkable improvement in the forecasts of TCs using Numerical Weather Prediction (NWP) models. These improvements are due to the improvement in the resolution, data assimilation techniques as well as the physics of the NWP models (Mandal et al., 2003; Ashrit et al., 2006, Pattanayak et al., 2010; Osuri et al., 2013; Mohapatra et al., 2013; Routray et al., 2017a&b; Heming et al., 2019; Dutta et al., 2019). There have been several studies involving the global models for tropical cyclone forecasting. An exhaustive review is not attempted in this paper. TC analysis and forecast improvements demonstrated by assimilation of OSCAT surface winds in a global model (T574L64; Prasad et al., 2013) is one of the early demonstrations at NCMRWF using the global forecast model for TC. Usually, global NWP models, due to their coarser-resolution, cannot predict the intensity of the TC. Therefore a regional model with higher resolution and explicit convection is used. In an early study, Mandal et al. (2003) showed the improvement in the TC track forecasts over Bay of Bengal cyclones using a modified version of the regional model developed in collaboration with the Naval Research Laboratory (NRL) and North Carolina State University. Improved prediction of TC cases is due to increased resolution and assimilation of satellite data is also reported by Srinivas et al. (2010, 2012). Osuri et al. (2013), in their study, have compared the 18 and 9 km version of the Advanced Research version of Weather Research and Forecasting (ARW) model and show that the 9 km version has lower track errors with better intensity prediction. Impact of cyclone bogusing and data assimilation using WRF ARW (Chourasia et al., 2013), improved forecast of cyclone Phailin with 4DVAR assimilation (Iyengar et al., 2014), sensitivity to different convective parameterization schemes (Saji and Ashrit, 2014), the impact of assimilating Megha Tropiques SAPHIR radiances on tropical cyclone forecasts using WRF (Dhanya et al., 2016) are some of the important studies involving Bay of Bengal cyclones. Das et al. (2015) provides the first compilation of HWRF evaluation for North Indian Ocean tropical cyclones for all the cases during 2010-2013. The study based on nine TC cases showed an average track that displayed an improvement of 7, 27, 25 and 15% over the IMD operational forecasts at 36, 48, 60 and 72 h, respectively. The model with a high-resolution 3 km nest displayed a significant improvement in track forecasts with 12-46% over the model with a 9-km resolution nest. However, the HWRF model intensity forecasts showed only a marginal improvement of 5-8% over the IMD operational forecasts [Nadimpalli et al. (2020)]. Besides an improved intensity forecast, high-resolution regional models can predict the finer structure of a TC. The prediction of Bay of Bengal cyclones through assimilation of Doppler weather radar observations (Osuri et al., 2015) and prediction of rapid intensification (RI) using HWRF for the case of Phyllis (Osuri et al., 2017) have improved. More recently using the Hurricane WRF (HWRF), Nadimpalli, et al. (2020) have demonstrated improved performance of HWRF against the quasi-operational WRF model forecasts of tropical cyclones over the Bay of Bengal. An evaluation carried out for 10 cases from 2013 to 2017 found a 27% improvement in skill over the quasi-operational WRF forecasts. The accurate prediction of TC's structure during landfall helps assess the distribution of strong winds and heavy rainfall, which can extend further inland, causing floods (Leroux et al., 2018). Several advances have been made in predicting a cyclone's structure in recent times (Heming and Goerss, 2010; Hazelton et al., 2018). Hazelton et al. (2018) have used a nested version of the finite-volume dynamical core (FV3) with GFS physics (fvGFS) to show that this model has the capability of predicting TC intensity and structure more accurately.

Super Cyclonic Storm (SuCS) Amphan was the first cyclone for the pre-monsoon cyclone season of 2020. It caused widespread damage over India's eastern part (particularly West Bengal, where it made landfall) during the period. As per the preliminary estimates (reported in media; CNN), total damage was estimated to be around 13.7 Billion USD. However, due to the Government of India's timely preparations, the loss of life was limited to 86. According to the India Meteorological Department (IMD), this was the strongest TC to occur in the BOB since the 1999 Odisha SuCS. Coastal areas of Odisha, particularly Paradeep, received extremely heavy rainfall amounts (>200 mm) of 24 hrs accumulated rainfall during 19-20 May, 2020 (IMD tropical cyclone bulletin of 20th May, 2020).

In this study, we have analysed the performance of the National Centre for Medium Range Weather
## TABLE 1

NCMRWF Unified Model configuration since June 2018

| Model | Application & domain | Resolution | Forecasts |
|-------|----------------------|------------|-----------|
| NCUM-G | Global Deterministic Model | N1024L70 (12 km horizontal resolution with 70 vertical levels) | 0000 UTC : Day 1 to Day 10 1200 UTC : Day 1 to Day 10 |
| NCUM-R | Regional Deterministic Model high resolution over Indian region (540° N and 65100° E) | 4 km resolution  Explicit convection | 0000 UTC : Day 1 to Day 3 1200 UTC : Day 1 to Day 3 |

## TABLE 2

Observations Assimilated in NCUM Global Data assimilation system

| Observation type | Observation description | Assimilated Variables |
|------------------|-------------------------|-----------------------|
| AHIClear | Advanced Himawari Imager radiances from Himawari-8 | Brightness Temperature (Tb) |
| Aircraft | Upper-air wind and temperature from aircraft | u, v, T |
| AIRS | Atmospheric Infrared Sounder onboard AQUA Satellite | Tb |
| AMSR | Radiances from AMSR-2 onboard GCOM satellite | Tb |
| ATOVS | AMSU-A (all sky), AMSU-B/MHS, HIRS from NOAA-18 &19, MetOp-A&B | Tb |
| ATMS | Advanced Technology Microwave Sounder in NPP satellite | Tb |
| CrIS | Cross-track Infrared Sensor observations in NPP satellite | Tb |
| FY3C | Radiances from Micro Wave Humidity Sounder (MWHS) of FY3C Satellite | Tb |
| GMI | Observations from Global Precipitation Measurement (GPM) Microwave Imager (GMI) instrument | Tb |
| GOES | Cloud clear Imager radiances from GOES | Tb |
| GOES | Global Positioning System Radio Occultation observations from various satellites (including MT-ROSA) | Bending Angle |
| Ground GPS | Ground based GPS observations from various locations | Zenith Total Delay |
| IASI | Infrared Atmospheric Sounding Interferometer from MetOp-A&B | Tb |
| INSAT-3D Sounder | INSAT-3D Sounder radiances | Tb |
| INSAT-3D Imager | Cloud clear Imager radiances from INSAT-3D | Tb |
| SAPHIR | SAPHIR microwave radiances from Megha-Tropiques | Tb |
| Satwind | Atmospheric Motion Vectors from various geostationary and polar orbiting satellites (including INSAT-3D) | u, v |
| Scatwind | Scattrometer observations (Ocean Surface Wind) from MetOp-A & B, ScatSat-1, WindSat | u, v |
| SEVIRIClear | Cloud clear observations from SEVIRI of METEOSAT 8 & METEOSAT 11 | Tb |
| Sonde | Radiosonde observations, upper-air wind profile from pilot balloons, wind profiles, VAD wind observation from Indian DWR | u, v, T, q |
| Surface | Surface observations from Land and Ocean | u, v, T, q, P |
| SSMIS | SSMIS Radiances from DMSP satellites | Tb |
Forecasting (NCMRWF) deterministic models in forecasting the Super Cyclone (SuCS) Amphan, which was observed during 16-21 May, 2020 over the Bay of Bengal (BOB). This study compares the forecast of increased grid resolution in the NCMRF high resolution (4 km) regional model (NCUM-R) and (12 km) global model (NCUM-G). Both the models are being operationally used at NCMRF for the numerical prediction of severe weather events over India. The NCMRF Unified Model (NCUM) has been adapted from the Unified Model (UM) of the "UM Partnership). More details about the NCUM modeling system are given in the next sub-sections.

1.1. NCMRF Unified Modelling system

The NCUM-G (Rajagopal et al., 2012; George et al., 2016) uses a seamless modeling approach, has a horizontal grid resolution of ~12 km and 70 vertical levels (reaching 80 km height), is being used for the 240 hrs numerical weather forecast since 2018 (Kumar et al., 2018a). This model and assimilation system have been updated periodically to adapt to various scientific and technical developments. Advanced END Game dynamical core is used in the model, which provides improved accuracy of the solution of primitive model equations and reduced damping. END Game also increases variability in the tropics, which leads to an improved representation of TCs and other tropical phenomena (Walters et al., 2017). An advanced data assimilation method Hybrid 4D-Var is used for the creation of NCUM global atmospheric analysis. Ensemble Transform Kalman Filter (ETKF) based on the NCMRWF ensemble prediction system (NEPS) provides flow-dependent background errors to this Hybrid 4D-Var system. Utmost importance has been given to the assimilation of Indian satellite observations in this data assimilation system. INSAT-3D Atmospheric Motion Vector (AMV), Megha Tropiques (MT)-SAPHIR radiance, Scatsat Ocean Surface Winds are being assimilated in the operational NCUM global data assimilation system, in addition to other global observations. A list of observations assimilated in the latest NCUM global data assimilation system is given in Table 2. Salient Features of NCUM Assimilation - Forecast System is shown in Table 3.

NCUM global data assimilation system produces analyses at 0000, 0600, 1200 and 1800 UTC. In each 6 hourly data assimilation cycle, the available observations distributed over the 6 hour assimilation window (center of the analysis cycle ± 3 hr) are combined with the model background to produce the NCUM-G analysis. Table 1 summarizes the model configurations operational at NCMRF. Details on the model parameterization schemes, data assimilation, etc., can be found in Kumar et al. (2018b).

NCUM-R has a horizontal grid resolution of ~4 km and 80 vertical levels, with the model top at 38.5 km and 14 model levels below 1 km. The model has a time step of 1 minute. The model domain covers India and the adjacent oceanic regions and is operationally producing 72 hrs forecasts. In this convection-permitting model configuration, sub-grid scale deep convection is not parameterized. The prognostic cloud fraction and prognostic condensate (PC2) scheme used in this model is based on Wilson (2008a&b). The sub-grid turbulence scheme used is a blended scheme (Boutle et al., 2014), which dynamically combines the one-dimensional (1D) boundary-layer scheme of Lock et al. (2000) with a 3D
Smagorinsky scheme using a mixing factor of 0.5. The model employs NASA Shuttle Radar Topographic Mission (SRTM) 90 m digital elevation map orography.

NCUM-R uses the high resolution analysis prepared by the 4D-Var data assimilation (DA) system. In addition to most of the observations used in the NCUM global data assimilation system (even though data thinning strategies are different), Indian Doppler Weather Radar observations of radial wind are also used in the regional DA system with a time window of ± 3 hours. The model domain covers the South Asian region, covering BOB and part of the Arabian Sea (6° S -41° N and 62-106° E). The details of NCUM-R model configuration can be found in Dutta et al., 2019; Jayakumar et al., 2019 and Bush et al., 2020.

1.2. Variational data assimilation

Data assimilation based on the 4D-Var method has been used to prepare an analysis (initial condition) for NCUM since 2012. A detailed description of the 4D-Var system can be seen in Rawlins et al. (2007); Rajagopal et al. (2012); John et al. (2016) and Kumar et al. (2018b). The 4D-Var system produces the analysis by minimizing a cost function (penalty function), which describes the departure of the analysis from background and observations. The 4D-Var uses the information of "background" or “first guess” (a short forecast from previous analysis), observations, as well as error statistics of background and observations. A drawback of 4D-Var is that the background error used in the system does not account for the day-to-day varying model errors due to the changes in the weather conditions. One way to include the everyday varying forecast error is by using ensemble forecasts to calculate the forecast uncertainty. So in 2016, the data assimilation system was upgraded to Hybrid 4D-Var (Kumar et al., 2018a). The Hybrid 4D-Var system's advantage is that it uses "varying day-to-day flow-dependent" background errors in addition to "climatological" background errors. The Ensemble transformer Kalman Filter (ETKF) based ensemble prediction system at NCMRWF provides flow-dependent background errors to the Hybrid 4D-Var system. After that, improvements have been made in the data assimilation system to assimilate newer observations available with the global observing system. Utmost importance has been given to the assimilation of Indian satellite observations. Indian satellite observations of INSAT-3D imager and sounder radiance, INSAT-3D Atmospheric Motion Vector (AMV), Megha Tropiques (MT)-SAPHIR radiance, MT-ROSA Radio Occultation (RO), Scatsat Ocean Surface Winds are being assimilated in the latest operational NCUM Hybrid 4D-Var global data assimilation system. A list of observations assimilated in the latest NCUM global data assimilation system is given in Table 2. Salient features of NCUM-G Assimilation - Forecast System is provided in Table 3.
2. **NCUM Global and regional analysis**

The space-time evolution of Amphan cyclone in NCUM global and regional analysis is shown in Figs. 2&3 via the mean sea level pressure (MSLP) and 850 hPa winds. Observed cyclone track (solid black line) is also indicated in each panel to compare cyclone position in the model analysis. The performance of NCUM-G analysis and forecasts during the cyclone is discussed in terms of MSLP and 850 hPa level winds. It can be seen that global and regional analyses represented the system from the stage of a well-marked low-pressure system and its intensifications are reasonably well represented during the life-span of the cyclonic storm. During 16-17 May, 2020, within 12 hours or less, the system became more distinct as it gradually intensified into a depression,
gaining from a prolonged stay over warm oceans. The system has spiral bands of deep convective clouds surrounding the system's low-pressure center, as evidenced by the streamlines (Fig. 3). Despite having a different resolution, the cyclone's intensity in analysis, in terms of wind speed in both global (Fig. 3; top) and regional (Fig. 3; bottom), agree well. Enhanced circular isobars and wind speeds in both global and regional analysis indicate the storm's intensification on 17th May, 2020. A close correspondence in the movement and landfall also can be noticed from both the analysis.

3. NCUM Global and regional forecasts

In this section, a brief description of global and regional forecasts of the Amphan cyclone is discussed. When compared with the global analysis, the 24 hr (Day-1) forecast of MSLP and 850 hPa
Fig. 6. Observed and model forecast tracks for cyclone Amphan based on NCUM-G (top) and NCUM-R (bottom) are shown for 0000 UTC (left) and 1200 UTC (right) forecasts during 16-20 May, 2020.

winds (Fig. 4&5 respectively) show well-marked depression on 16th May, 2020, rapid intensification of the storm on 17th May, 2020, steady movement on the next couple of days and landfall on 20th May, 2020 agree well. As seen from the 850 hPa low-level winds, the intensity of the cyclone is also well predicted in global model forecasts (Fig. 5). Day-1 global NCUM forecasts on 18th May, 2020 show the system's North-west ward movement and landfall occurrence on the 20th May, 2020. Subsequently, Day-3 forecasts show the system has made a further inward movement towards land and located over west Bengal (not shown). As it moved further inland, it rapidly weakened. The storm was downgraded into Category 1, equivalent to Cyclonic Storm (CS), just six hours after landfall and became disorganized. On the other hand, the regional NCUM forecasts slightly overestimate the intensity at all the forecast times.

Further, in the regional NCUM, the center of the cyclone is slightly located south-eastward compared to the respective analysis and the IMD best track position (solid black line). This intensity overestimation in the regional NCUM Day-1 forecast is also evident in the winds (Fig. 5). It is interesting to note that the cyclone movement meanders in the regional model forecast compared to the best track with the lead time. For example, the cyclone center is situated on the westward side of the best track position during the rapid intensification period (on 17th May, 2020). In contrast, it moved to the east side of the track in the subsequent days.

4. Cyclone forecasts and its verification

The verification of cyclone forecasts involved evaluating the forecast tracks and intensity against the best track (BT) estimated. Additionally, verification of landfall position and time is also presented in this section based on the reported landfall position and time. Verification of Rapid Intensification (RI) of the SuSC Amphan is also assessed in the forecasts using the 24-hour change in the predicted wind speed by the models.

4.1. The bi-variate TC Tracker

The UK Met Office bi-variate approach to tracking TCs is used to track the location of the Super Cyclone ‘Amphan’. The bi-variate method identifies TCs by examination of the 850 relative vorticity field but then fixes the TC center to the nearest local MSLP minimum (Heming, 2017). The method’s key advantage is that it gives a strong indication of the approximate center of the TC even for weak systems and does not depend on the ‘TC-Vitals’ information for tracking.

4.2. Observed and predicted tracks (0000 and 1200 UTC)

Track predictions obtained for the cyclone ‘Amphan’ from NCUM-G and NCUM-R based on various initial conditions (ICs) from 16-20 May, 2020 during 0000 and 1200 UTC are shown in Fig. 6. Though the cyclone track predictions from both NCUM model versions (global and regional) depict slight discrepancies with varying ICs compared with the IMD best track (black curve), most of the track forecasts indicate the cyclone landfall over West Bengal and Bangladesh regions. Compared with the IMD track, cyclone track prediction is more accurate and consistent in Day-1 (green) and Day-2 (purple) from NCUM-G and NCUM-R, which were initialized with 18-19 May, 2020 analysis, respectively. Track forecast based on 0000 and 1200 UTC of 16th May, 2020 in NCUM-G (0000 and 1200 UTC NCUM-R) indicates the
highest error, with the track being much to the east of the observed track. Similarly, the track forecast based on 17th May also is shifted eastwards; however, with an improved track compared to the track predicted based on 16th May.

4.3. Forecast track errors

The NCUM-G and NCUM-R tracks based on 0000 and 1200 UTC forecasts from 13-20 May, 2020 have been used in the verification. Table 4 summarizes the track errors at different lead times. The track error components of the direct position error (DPE), along track error (ATE) and cross track error (CTE), are shown in Fig. 7. The computation of DPE, ATE and CTE follows the method described in Heming (2017). It is noted that the early forecasts during 16th and 17th May, 2020 predicted the track much to the east of the observed track (Fig. 6), which is reflected in high CTE values at higher lead times.
### TABLE 4
Forecast Track Errors for SCS Amphan from 13-21 May, 2020. NCUM-G, NEPS-G and NCUM-R track errors are based on 0000 UTC and 1200 UTC (numbers in the brackets indicate number of cases).

| Forecast Hour | 0    | 24   | 48    | 72   | 96   | 120  |
|---------------|------|------|-------|------|------|------|
| NUCM-G        | 43 (10) | 68 (12) | 112 (12) | 183 (11) | 210 (10) | 250 (8) |
| NCUM-R        | 48 (11) | 78 (12) | 99 (12) | 153 (11) | -     | -     |

### TABLE 5
Forecast track errors before the naming of the cyclone (13-15 May, 2020) and after the naming of cyclone (16-21 May, 2020).

| Forecast Hour | 0 | 12 | 24 | 36 | 48 | 60 | 72 | 84 | 96 | 108 | 120 |
|---------------|---|----|----|----|----|----|----|----|----|-----|-----|
| NUCM-G        |   |    |    |    |    |    |    |    |    |     |     |
| NCUM-G        |   |    |    |    |    |    |    |    |    |     |     |
| NCUM-R        |   |    |    |    |    |    |    |    |    |     |     |

### TABLE 6
Error in the forecast landfall time and position (Forecast time – Observed time) [-ve = early +ve = delay]

| IC             | NUCM-G | NUCM-R |
|----------------|--------|--------|
|                | Time error (hr:min) | Position error (km) | Time-error (hr:min) | Position error (km) |
| 0000 UTC 16052020 | -11:00 | 263 | - | - |
| 1200 UTC 16052020 | -07:30 | 200 | - | - |
| 0000 UTC 17052020 | -04:00 | 105 | - | - |
| 1200 UTC 17052020 | -03:30 | 200 | -04:00 | 145 |
| 0000 UTC 18052020 | 01:00 | 143 | -00:30 | 57 |
| 1200 UTC 18052020 | -03:30 | 23 | -00:30 | 26 |
| 0000 UTC 19052020 | -02:00 | 37 | 00:00 | 0 |
| 1200 UTC 19052020 | -01:00 | 12 | 00:00 | 12 |
| 0000 UTC 20052020 | -00:30 | 8 | 1:30 | 5 |
The mean initial position error is lowest in NCUM-G at 43 km. The 24 hr DPE ranges between 48-68 km, the 48 hr DPE ranges between 99-133 km and the 72 hr DPE ranges from 153-197 km. The DPE computed based on the forecasts for 13-15th May (Table 5) indicates lower values than the DPE values based on forecasts during 16-20 May, 2020. This possibility suggests higher DPE during and after the intensification of the cyclone.

### 4.4. Forecast landfall position and time errors

Forecast errors in landfall time and position from NCUM-G and NCUM-R are showed in Table 6. Forecasts made on 16th May, 2020 had relatively large errors both in landfall position (>200 km) and time of over 7-11 hours (early). Large position errors in forecasts with ICs before 0000 UTC on 18th May are consistent with large CTE
shown in Fig. 7. This is evident in the CTE magnitudes at 36-60 hour lead times. The time error has reduced to 1.3-7 hours (early) for forecasts based on 17th May, 2020 IC and the landfall position errors are also lower. Nevertheless, the forecasts made after 0000 UTC 18th May, 2020 have an extremely low error in both landfall position and time (Table 6). This is consistent with low ATE values at lead times of under 30 hours in Fig. 7. The forecasts from NCUM-R show the least error in space and time.

4.5. Forecast intensity

The minima in SLP and maxima in winds indicate the intensity of the cyclone. The observed and forecast Minimum SLP and Maximum Winds are shown in Fig. 8. Delayed peak intensity is evident in the forecasts. The NCUM-R predicted (66 hrs) Minimum SLP based on 16th May, 2020 initial condition is close to the observed intensity of 920 hPa on 18th May, 2020 at 1800 UTC. However, the forecasted Maximum Wind speed of 102 kt is much lower than the observed magnitude of 125 kt. It is evident from Fig. 8 that the model forecasts consistently indicated delayed intensification. The mean absolute error (MEA) in Minimum SLP and Maximum Wind is shown in Fig. 9. The highest SLP errors at 24, 48 and 72-hour forecasts are in NCUM-R. The lowest errors are evident in NCUM-G. The MEA in the Max Wind in NCUM-G and NCUM-R are very close, suggesting no significant advantage of high resolution in this case.

The bias can also be seen in forecast pressure-wind curves shown in Fig. 10. For every forecast, both the model predicted and observed Min SLP and Max 10-m winds are paired at a specified lead time. Black, filled dots indicate observed pressure-wind pairs, while red and blue filled dots indicate particular forecasts from NCUM-G and NCUM-R, respectively, at the specified lead time. The scatter points from observations and forecasts tend to overlay when the system is weak. With increasing intensity, the forecasts tend to show growing bias (lower Min SLP and lower Max Winds).

4.6. Rapid Intensification (RI)

The RI is defined as an increase of intensity of about 30 kt (15.4 ms$^{-1}$) in 24-h (IMD, 2015). As per the IMD official reports on 16th May, the system intensified from Depression (D) to Deep Depression (DD) and Cyclonic Storm (CS) on the same day. Moving nearly northwards, it further intensified into a Severe Cyclonic Storm (SCS) over southeast BoB in the morning of 17th May. It underwent rapid intensification (RI) during the next 24 hours and accordingly intensified into a Very Severe Cyclonic Storm (VSCS) by the afternoon of 17th May, Extremely Severe Cyclonic Storm (ESCS) in the early hours of 18th and into a SuCS around noon of 18th May, 2020. The forecasts show very strong intensification (Fig. 8) in both the global (NCUM-G) and regional (NCUM-R) model. However, the time of intensification is slightly different compared to the observations. The 24-hour change in the observed Max Wind associated with the cyclonic system is shown in Figs. 10(a&b). As reported, the cyclone underwent RI during 17-18 May, 2020, reflected in the obs (black) in Figs. 10(a-c). The 24-hour change in the reported Max wind remains higher than 30 kt from 0000 UTC on 17th May to 1800 UTC on 18th May. The NCUM-G forecasts, although they showed substantial intensification (Fig. 8), do not predict RI (NCUM-G Forecast based on 15th May comes closest to predicting the RI but misses by a narrow margin). The other forecasts rather show relatively gradual and rather late intensification.
On the contrary, the NCUM-R forecasts show improved performance in predicting the RI. In the forecast based on 15th May, NCUM-R predicts RI at 0600 UTC on 17th May. Forecast based on 16th May also predicts RI at 1200 UTC on 18th May, much closer to the actual time of intensification, although late by few hours. Again the forecast based on 17th May, 2020 predicts RI at 0000, 0600 and 1200 UTC of 19th May, 2020. Thus, it can be concluded that the high resolution (4 km) forecasts based on NCUM-R show relatively improved performance compared to NCUM-G in predicting RI on 15th, 16th and 17th May, 2020.

5. Cyclone structure

Structure of TC in NCUM-G (12 km) and NCUM-R (4 km) forecasts are discussed here. An example of the structural differences arising from resolution differences
in the forecast of TC is shown in Figs. 12(a-h). The panels in the top row (Figs. a, c, e & g) correspond to NCUM-G and the panels in the bottom row correspond to NCUM-R. All the plots correspond to 72-hour forecast based on 17th May, 2020. In the high-resolution NCUM-R, the 850 hPa vorticity core of cyclone Amphan becomes much stronger and possesses a more horizontal structure [Fig. 12(b)] compared to the NCUM-G (12 km) forecast [Fig. 12(a)]. Similar results are evident for both 850-hPa horizontal wind [Figs. 12(c&d)] and low-level cloud fraction [Figs. 12(e&f)], with the 4 km model generating stronger winds with, much tighter storm core and a cloud free eye as well as spiral rain bands branching off the central dense overcast region at the core of the cyclone [Fig. 12(e&f)]. The 12-km NCUM-G grid shows a relatively weaker, broader cyclonic structure. Lastly, the higher resolution of the NCUM-R allows for more intense updrafts at the 500 hPa level, with a corresponding downdraft in the eye region [Figs. 12(a-h)]. Strength of vertical motion is associated with the spiral rain bands can be assessed from Low-Level Cloud Fraction. The unrefined forecast in NCUM-G shows a relatively larger, weaker peak in vertical motion with only one ascent band present around the storm core [Fig. 12(g)]. The high resolution forecast in NCUM-R shows stronger and multiple peaks of vertical motion [Fig. 12(h)].

[Figs. 13(a-d)] show a snapshot of the azimuthally averaged vertical cross-section of tangential (top) and radial wind (bottom) in NCUM-G (left) and NCUM-R (right) in the 72-hour forecast initialized with 0110 UTC 17th May, 2020 analysis. The storm’s wind speed minimum defines the center of the cross-section. The structural differences resulting from the model grid resolution is seen in this figure. Both surface radial inflow (negative values) and upper-level outflow (positive values) are stronger in NCUM-R [Fig. 13(e)] when compared to NCUM-G [Fig. 13(d)], indicative of a much stronger circulation associated with the cyclone. The NCUM-G forecast [Fig. 13(c)] shows a more vertically diffuse inflow core, indicating that near-surface momentum may not be as concentrated in the model’s lowest levels, thereby decreasing the efficiency of taking sensible and latent heat energy from the ocean surface. This is also shown in the tangential wind [Figs. 13(a&b)], which indicates a higher maximum wind location with NCUM-R. Besides, NCUM-R exhibits tangential wind structure similar to that of traditional, strong TCs (calm
Figs. 14(a-d). Azimuthally averaged vertical cross-section of temperature anomaly (top) and vertical velocity (bottom) in NCUM-G (left) and NCUM-R (right) in the 72-hour forecast valid 0000 UTC 20th May, 2020. Positive shaded region in top panels indicate warm core region. Positive shaded regions in the bottom panels indicate region of strong upward motion.

eye, sloped eyewall near-surface maximum wind). In contrast, the TC's structure in NCUM-G is less organized, with a radius of maximum wind approximately greater than that of NCUM-R.

[Figs. 14(a-d)] show a snapshot of the azimuthally averaged vertical cross-section of temperature anomaly (top) and vertical velocity (bottom) in NCUM-G (left) and NCUM-R (right) of 72-hour forecast initialized at 0000 UTC 17th May, 2020. The temperature anomaly [Figs. 14(a&b)] clearly shows the cyclone's warm core structure much more organized in NCUM-R. The vertical pressure velocity [Fig. 14(c&d)] also highlights the intensity differences between model runs. NCUM-R shows a deep, penetrating updraft core in the eyewall, whereas NCUM-G shows a much broader, weaker, more tilted updraft. Thus, the impact of high-resolution NCUM-R forecasts in improved representation of the cyclone intensity and structure is evident from the figures.

6. Summary

This study focused on comparative analysis of the recent SuCS ‘Amphan’ forecasts by assesses 4 km regional model NCUM-R and 12 km resolution global model NCUM-G. Both the models are operationally being used at NCMRWF for NWP. The findings of this study can be summarized as follows.

(i) The space-time evolution of SuCS ‘Amphan’ in NCUM global and regional analyses is realistic even from the early stage of a well-marked low-pressure system. Further, during its intensification and its life-span as the intense cyclonic storm, the two analyses capture the system reasonably well. Similarly, the forecast track and intensity of the SuCS Amphan are well captured in the global and regional models accurately up to three days in advance and reasonably well up to five days.

(ii) Track error statistics show that the mean initial position errors in the global (43 km) and regional (48 km) models are very close. However, the 24, 48 and 72-hour forecast position errors in global (NCUM-G) are 68, 112 and 183 km, respectively, which are higher than errors of 78, 99 and 153 km of NCUM-R. Forecast track errors based on earlier initial conditions (13-15 May, 2020) are higher than the errors based on the initial condition after the formation of D onwards (16-21 May, 2020).
(iii) Predicted landfall position (and time) errors are greater than 200 km (and about 3–11 hours late) in forecasts based on the ICs before 0000 UTC of 17th May, 2020. This is subsequently reduced to less than 50 km (30 min to 3 hr late) in the forecasts after 0000 UTC 18th May, 2020. NCUM-R forecasts feature the least error in landfall position (0 to 26 km) and time (30 min late to 0130 min early).

(iv) Time delay in attaining the peak intensity is noticed in the forecasts compared to observations. The NCUM-R predicted Minimum SLP based on 16th May, 2020 is close to the observed intensity of 920 hPa on 18th May, 2020 at 1800 UTC. However, the maximum forecast wind is 102 kt is lower compared to the observed 125 kt. It is found that the model predicted intensity is more realistic when the system is weak. However, with the increase of the observed intensity, the forecasts tend to show growing biases.

(v) As per the IMD reports, SuCS Amphan underwent rapid intensification (RI) from 17-18 May, 2020. Both global (NCUM-G) and regional (NCUM-R) models indicate strong intensification, although not at the right time compared to the observations. The NCUM-G forecasts, although they showed strong intensification, do not predict RI (NCUM-G Forecast based on 15th May is closest in predicting the RI but misses by a narrow margin). NCUM-R forecast based on 15th (& 16th) of May predicted RI at 0600 UTC on 17th May (& 1200 UTC on 18th May). The RI predicted by NCUM-R at 1200 UTC on 18th May, is much closer to the reported timing, although late by few hours. Again the forecast based on 17th May, 2020 predicted RI at 0000, 0600 and 1200 UTC on 19th May, 2020.

(vi) Concerning track forecast, both NCUM-G and NCUM-R shows an impressive and significant reduction in errors. However, for predicted intensity forecasts both global and regional models feature strong and delayed intensification. It is found that accurate representation of intensity in the initial conditions still has scope for improvement.

(vii) An investigation of the structural differences in the TC forecast arising from resolution differences is further carried out. It is found that the high-resolution NCUM-R forecasts show the 850 hPa vorticity core (850 hPa wind, low-level cloud fraction, more intense updrafts at 500 hPa) of the cyclone Amphan, which is much stronger and possesses more horizontal structure with cloud free eye compared to the 12 km resolution NCUM-G.

(viii) Azimuthally averaged vertical cross-sections of tangential and radial wind forecasts from NCUM-G and NCUM-R are assessed for a deeper understanding of the structural differences resulting from the model grid resolution. Stronger surface radial inflow (and upper-level outflow) in NCUM-R is indicative of a much stronger circulation. NCUM-R exhibits a tangential wind structure similar to traditional, strong TCs (calm eye, sloped eyewall near-surface maximum wind). In contrast, the NCUM-G TC structure is less organized, with a radius of maximum wind greater than that of NCUM-R.

(ix) Vertical cross-section of temperature anomaly clearly shows that the cyclone's warm core structure's warm core structure is much more organized in NCUM-R. The cross-section of vertical pressure velocity field also highlights the intensity differences between model forecasts of NCUM-R and NCUM-G, where NCUM-R shows a deep and penetrating updraft core in the eyewall, which is missing in NCUM-G.

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