Photometric properties of magnetic elements: resolved and unresolved features

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Abstract. We investigate, by numerical simulations, the photometric signature of magnetic flux tubes in the solar photosphere. We show that the observed contrast profiles are determined not only by the physical properties of the tube and its surroundings, but also by the peculiarities of the observations, including the line/continuum formation height and the spatial and spectral resolution. The aim is to understand these contributions well enough so that multi-wavelength observations can begin to disentangle them.

1. Introduction
The high spatial resolution achieved by modern telescopes, along with improvements in real time and post-processing correction of image degradation, has allowed the detailed study of the photometric properties of small magnetic bright points. Nevertheless, significant disparities exist in measurements of the contrast as a function of disk position (center-to-limb variation or CLV). Moreover, recent observations off disk center have shown that small magnetic features are often associated with the presence of 'dark lanes' and 'bright tails' (Lites et al. 2004; Hirzberger & Wiehr 2005; Berger et al. 2007), which are manifestations of thermal effects induced by the reduction of opacity inside the magnetic elements (Steiner 2005). In this paper, we demonstrate how the photometric signatures of small magnetic elements reflect, not only the physical properties of the flux tube and its surroundings, but also the peculiarities of the observation itself (such as spatial resolution and spectral range).

2. The Model
We investigate, by 2D numerical simulations, the radiative properties of isolated and clustered static magnetic flux tubes in Radiative Equilibrium (RE, hereafter) with a surrounding plane parallel gray atmosphere. LTE is assumed. RE is imposed by an iterative scheme similar to the one proposed by Fabiani Bendicho et al. (1992). The radiation intensity field is evaluated by a code (Criscuoli, 2007\footnote{See \url{http://dspace.uniroma2.it/dspace/advanced-search/}} based on the short characteristic technique (Kunasz & Auer 1988). As initial conditions for atmospheric parameters, the Kurucz model (Kurucz 1994) is adopted. The presence of the magnetic field is mimicked by shifting downward
the atmosphere at the flux tube location. The spatial domain of the simulations is $1.1 \times 2.3 \text{Mm}$ with horizontal and vertical resolution of $3.5 \text{km}$ and $7.1 \text{km}$, respectively. The magnetic field intensity is estimated, at each height, supposing the thin flux tube approximation (Stix 2002). An example of the simulated temperature field inside and around a flux tube in RE is given in fig.1. Because of the reduction of opacity in the magnetic element, at large optical depths ($\tau \geq 1$) the temperature inside and immediately outside the tube is lower than the surroundings. At the shallower optical depths ($\tau < 1$), due to the radiative channeling effect (Fabiani Bendicho et al. 1992), the tube and the adjacent atmosphere are hotter.

3. Formation height

Because the thermal stratification depends on the height (see fig.1), the contrast across magnetic elements is different when observed at wavelengths which sample different layers of the atmosphere. In our gray models this effect is investigated
by comparing the contrast across a magnetic flux tube obtained by modifying the model adopted for the opacity. Figure 1 shows \( \tau = 1 \) lines at various lines of sight (\( \mu \) is the cosine of the heliocentric angle) in the case of the Rosseland mean opacity from Kurucz model (dashed lines) and in the case in which the opacity is increased by a factor of two (dotted lines). Figure 2 shows the corresponding contrast profiles. At \( \mu = 1 \) the Wilson depressions are approximately 60km in both cases, but the contrast is higher in the case of higher opacity, because the corresponding iso-optical line samples layers at which the temperature gradient is larger. Both plots show 'double humps' and 'dark rings', whose origin is discussed by Knöllker et al. (1988). Because of the heating in the highest layers of the domain, the temperature difference between the 'wall' and the non-magnetic atmosphere decreases monotonically with increasing the line of sight angle. Therefore, the maximum contrast value decreases monotonically with decreasing \( \mu \) for the higher opacity model.

4. Resolution, Clustering and Identification methods

Figure 3 shows the contrast profiles observed at various positions on the solar disk and different resolutions for three flux tubes in RE with the surrounding atmosphere and whose mutual distances (from tube axis) and diameters are 105km and 70km, respectively. Boundary and initial conditions are as for the tube in fig.1. The central and right plots show contrast profiles obtained convolving original profiles with Gaussian functions of FWHM=0.1" and FWHM=0.3", respectively. Figure 3 shows that there is a 'critical line of sight' beyond which the flux tubes are not distinguishable and appear as a single structure. Comparison of fig.1 and 3 shows that the contrast of clusters of magnetic elements is higher than the contrast of isolated elements. Finally, we notice that reduction of resolution mostly affects profiles observed at disk center, since these are characterized by features of spatial scales of tens of kilometers.

In fig.4 we show CLV obtained by 4 different observing conditions and features definitions for an isolated flux tube of 175km diameter (left) and three flux tubes of 70km diameter and 105km apart (right): 1) Maximum contrast observed with spatial resolution 0.1" (dashed lines); 2) Mean contrast of elements whose contrast is larger than a threshold and observed with spatial resolution
Figure 4. CLV of contrasts of isolated (left) or three flux tubes (right) measured at different spatial resolution and with different methods. Boundary conditions are such that, when in RE, the magnetic flux measured with spatial resolution worse than 0.4” is approximately the same for the two configurations. Legend is explained in the text.

0.1” (continuous line); 3)Mean contrast observed with spatial resolution 0.4”; 4)Mean contrast observed with spatial resolution 0.6” (dotted line).

The figure shows that the CLV of measured contrast of magnetic features depends on the image spatial resolution and on the technique employed to detect and define the features themselves. For instance, the two dotted curves of the two plots display different shapes and contrast values, although the magnetic field intensities of the three flux tubes are such that for resolution worse than 0.4 the magnetic flux measured is the same as for the isolated flux tube case. Therefore, methods based on magnetograms intensity thresholding would not distinguish between the single and the three flux tubes cases, thus producing a large spread of measured contrast.

5. Conclusions

We have showed, by 2D simulations, that measured intensity contrast of magnetic elements depends not only on their physical properties, but also on the peculiarities of the observations and on the data analysis techniques employed. Results obtained by this work will be useful for the interpretation of present and future high resolution observations, as well as for the interpretation of the discrepancies of some results presented in the literature.

References

Berger, T. E., Rouppe van der Voort, L., Löfdahl, M. 2007, A&A, 661, 1272
Criscuoli, S. 2007, Ph.D. thesis, University of Rome “Tor Vergata”
Fabiani Bendicho, P., Kneer, F. & Trujillo Bueno, J. 1992, A&A, 264, 229
Hirzberger, J. & Wiehr, E. 2005, A&A, 438, 1059
Knölker, M., Schüssler, M. & Weisshaar, E. 1988 A&A, 194, 257.
Kunasz, P.B., Auer, L.H. 1988, J. Quant. Spectroscop. Radiat. Transfer, 39, 67
Kurucz, R.L. 1994, CD-ROM No. 19
Lites, B. W., Scharmer, G. B., Berger, T. E., Title, A. M. 2004 , Solar Physics, 221, 65
Steiner, O. 2005, A&A, 430, 691
Stix, M. 2002, The Sun: An Introduction, 2nd edition (Berlin: Springer)