Chapter 1

Community detection and role identification in directed networks: understanding the Twitter network of the care.data debate

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With the rise of social media as an important channel for the debate and discussion of public affairs, online social networks such as Twitter have become important platforms for public information and engagement by policy makers. To communicate effectively through Twitter, policy makers need to understand how influence and interest propagate within its network of users. In this chapter we use graph-theoretic methods to analyse the Twitter debate surrounding NHS England's controversial care.data scheme. Directionality is a crucial feature of the Twitter social graph - information flows from the followed to the followers - but is often ignored in social network analyses; our methods are based on the behaviour of dynamic processes on the network and can be applied naturally to directed networks. We uncover robust communities of users and show that these communities reflect how information flows through the Twitter network. We are also able to classify users by their differing roles in directing the flow of information through the network. Our methods and results will be useful to policy makers who would like to use Twitter effectively as a communication medium.

1. Introduction

The care.data programme is a scheme proposed by NHS England for collating patient-level data from all GP surgeries in England into a centralised national Health and Social Care Information Centre (HSCIC) database. This scheme would complement existing hospital records to create a linked primary- and secondary-care database, which could be used for improving healthcare provisioning and for medical research. The potential benefits of such a database are well-recognised, however, poor communication...
prior to the roll-out of the scheme in early-2014, alongside concerns around privacy, data security, and the possibility of the sale of data, led to the eventual postponement of the scheme. In the months leading up to the initial roll-out, these issues had become a major topic amongst Twitter users interested in healthcare as well as data privacy issues.

Twitter is a popular social network that allows users to post and read short messages with fewer than 140 characters. With 300 million active monthly users, it has become an influential digital medium for debates, mobilising support or opposition, and directing people towards other online material. Twitter thus provides a means for policy makers to engage with the general public and to use it as an effective communication platform, alongside more traditional methods of public engagement. In order to use Twitter effectively, it is important to understand how information and influence spreads within its network of users. The flow of information through Twitter depends on the pattern of connections between users, i.e., what Twitter calls the ‘social graph’. Tweets from a particular user appear on the ‘timeline’ of that user’s ‘followers,’ and these followers are then able to respond or ‘retweet’ the message, propagating the information on to their own followers. Within Twitter the directionality of links is therefore critically important; anybody is free to follow and retweet the President of the United States, but, for most users, to be retweeted by the President would be a significant event! It is clear that this asymmetry is a crucial ingredient defining how information propagates through the network.

Extracting information of the detailed directed structure of the Twitter social graph is therefore a key step towards understanding the evolution of a debate on a particular issue, particularly for policy makers who would like to reach the widest possible audience and effectively influence the debate. Concepts from graph theory and network analysis can be applied to address such questions. In particular, community detection is the graph-theoretical problem of identifying meaningful subgroups within a network. Within Twitter, this might correspond to groups of users who share similar interests, or who are engaging with each other on a particular topic. Although previous studies have used community detection methods to analyse Twitter networks, these have generally ignored the directionality of the edges. Indeed, most of the widely-used community detection methods are defined for undirected networks and are not easily adapted to the directed case.

In contrast, we use here two methods, Markov Stability and Role-
Based Similarity (RBS)\cite{20,21}, which are based on the behaviour of dynamical processes on the network and can thus be seamlessly applied to directed networks. Since they are flow-based, these methods naturally explore how information and influence propagate across the network of Twitter users, i.e., the communities and roles found by our analysis reflect the process of information spreading on the network. Markov Stability is a community detection method which identifies groups of nodes in the graph in which the flow of a diffusion process becomes trapped over a particular time scale\cite{18}. Role-based similarity finds groups of nodes based on the similarity of the in- and out-flow patterns, i.e., how flows enter and leave each node based on paths of all lengths. RBS thus provides a deeper insight into the flow roles of individual users within the network than traditional classifications into leaders and followers, or hubs and authorities. We have previously used these methods to analyse a network of influential Twitter users during the 2010 London riots.\cite{22}

In this chapter, we apply and extend these methods to analyse a set of tweets relating to the care.data programme, demonstrating how the information derived from graph-theoretical analyses of Twitter data can provide insight to policy makers on how to effectively engage with a Twitter audience. For a discussion of the implications of our research for policy makers see Ref.\cite{23}; here we present in greater detail the technical background to the analysis, as well as additional, extended results. We begin in Sections\ref{sec:maths} and\ref{sec:methods} by explaining the mathematics of the Markov Stability and Role-Based Similarity methods. In section\ref{sec:construction} we describe how we construct different directed networks of Twitter users from the set of tweets, based on declared interest (follower relationships) and active participation (retweets). We apply our methods to these networks in section\ref{sec:results} revealing the different communities involved in the care.data debate and the different roles played by users within the debate.

2. The Markov Stability community detection methodology

A frequent goal in network analysis is to partition the graph into meaningful subgroups, or communities, leading to a mesoscopic description of the network that can be extremely useful for making sense of large and complex data sets. The communities so obtained can also help reveal how global structure and function emerges from local connections. The literature contains a large number of methods for community detection (see Ref.\cite{11} for a review). The variety of community detection methods reflects
the fact that there cannot be a universal definition of what constitutes a ‘good’ partition of the network. However, most methods follow heuristics based on structural and combinatorial features of the network: typically a subset of nodes is thought of as a good community if the connections between the nodes within the subset are denser than the connections with nodes outside of the subset. Such heuristics are applied through optimisations of a variety of quality functions. A quality function based on this idea underlies the popular modularity method.

In addition to the well-known limitations of many of these methods, such as the ‘resolution limit’, the intrinsic presence of a particular scale, or the bias towards overpartitioning into clique-like communities, structural quality functions are not easily adapted to directed networks. On the other hand, the Markov Stability community detection method is based on the behaviour of dynamical processes on the network and, as such, it applies naturally to both undirected and directed networks. Furthermore, since Markov Stability is based on the flow of a Markov process on the graph, and not on structural features such as edge density, it can detect non-clique-like communities. Other methods have been proposed to detect communities based on diffusion processes, including Infomap and Walktrap, yet these methods do not concentrate on fully exploiting the transient information contained in the dynamics corresponding to the analysis of paths at all lengths. It is this dynamical zooming that allows Markov Stability to extract information of the graph at all scales and the plausibility of different coarse-grained descriptions of the graph over different time scales. For a full description of the method see Refs. Here we focus on the specifics of the application to directed networks; we start by outlining the necessary mathematical formalism for random walks on directed networks, and then introduce the Markov Stability quality function and discussing some practical issues related to its optimisation.

2.1. Random walks on directed networks and Markov Stability

2.1.1. Preliminaries

A directed graph with \( N \) nodes can be encoded by an \( N \times N \) adjacency matrix \( A \), where \( A_{ij} = 1 \) if there is a directed edge from node \( i \) to node \( j \), and \( A_{ij} = 0 \) otherwise. Nodes in directed graphs have an out-degree (given by the sum of rows of the adjacency matrix, \( d_{\text{out}} = A^{T}1 \)) and an in-degree (given by the sum of columns, \( d_{\text{in}} = A1 \)).
The evolution of the probability distribution of a simple discrete-time random-walk on a directed network defined by the (non-symmetric) adjacency matrix $A \neq A^T$ is given by
\[
p_{t+1} = p_t D^{-1}_{\text{out}} A = p_t M_{\text{dir}},
\]
where $p_t$ is a $1 \times N$ vector, $D_{\text{out}} = \text{diag}(d_{\text{out}})$, and $M_{\text{dir}} = D_{\text{out}}^{-1} A$ is the Markov transition matrix. If the graph is strongly connected (i.e., if any node can be reached from any other node) and aperiodic, then the random walk is ergodic with stationary distribution $\pi$, the dominant left eigenvector of $M_{\text{dir}}$, i.e., $\pi = \pi M_{\text{dir}}$. The entries of $\pi$ are the PageRank of the nodes in the graph, a well known variant of the eigenvector centrality which is used by the Google search algorithm.

In general, real-world networks will not be strongly connected and so the dynamics are not guaranteed to be ergodic. A common approach for ensuring the dynamics are ergodic is to use the ‘Google trick’ of random teleportation: if the random-walk is at a node with at least one out-link, then with probability $\alpha$ it will follow one of its outlinks, and with probability $1 - \alpha$ it will ‘teleport’ to a random node in the graph with uniform probability. If it is at a node with no out-links, then it will teleport with probability 1. The transition matrix for such a random-walk is
\[
M_{\text{dir}}(\alpha) = \alpha M_{\text{dir}} + [(1 - \alpha) I + \alpha \text{diag}(a)] \frac{11^T}{N},
\]
where $a$ is a dangling-node indicator vector ($a_i = 1$ if $i$ has no out-links and $a_i = 0$ otherwise). The customary value used for $\alpha$ is 0.85, which we adopt below. The equivalent continuous-time random-walk is governed by
\[
\dot{p} = -p \left( I - M_{\text{dir}}(\alpha) \right),
\]
and the transition matrix for the continuous time random-walk is then
\[
P(t) = \exp(-t(I - M_{\text{dir}}(\alpha))).
\]
as a subgraph on which the diffusion is well mixed and trapped over a given time scale. By allowing the random-walk to evolve for progressively longer times, the method acts as a ‘zooming lens’, uncovering structure (if present) at all scales. This dynamical zooming allows the method to extract a multi-resolution description without prescribing a scale for the partitions. In addition, the method can find not only the standard clique-like communities, but also non-clique communities, which are of interest in geographic, engineering and social systems.

Operationally, the method works by optimising a time-dependent quality function as follows. A particular partition of the network is represented by the $N \times c$ community indicator matrix $H$. Each row of $H$ corresponds to a node and each column a community: if node $i$ is in community $j$ then $H_{ij} = 1$ and the rest of row $i$ is zeros. We then define the clustered autocovariance matrix as

$$R(t, H) = H \left[ \Pi P(t) - \pi^T \pi \right] H^T := HQH^T,$$

where $\Pi = \text{diag}(\pi)$ and $P(t)$ is the random-walk transition matrix over time $t$ (e.g., for the discrete-time simple random walk this is $M_{\text{dir}}^t$). Note that in the undirected case, $Q = \Pi P(t) - \pi^T \pi$ is the actual autocovariance matrix of the diffusion process defined by $P(t)$, whereas for directed networks the matrix $Q$ is not symmetric and so it is not an autocovariance in the strict sense. The entries of the $R$ matrix have an intuitive interpretation in terms of the random-walk: $R(t, H)_{ij}$ is the probability of starting in community $i$ at stationarity and being at community $j$ at $t$ discounting the probability of two independent random-walkers being in $i$ and $j$ at stationarity. The diagonal entries $R(t, H)_{ii}$ can therefore be seen as a measure of the extent to which community $i$ traps the flow of the process over time $t$. The overall ‘quality’ of the partition, in terms of trapping the flow of the diffusion process, is the sum of these diagonal entries, and we define the Markov Stability of a partition as

$$r(t, H) = \text{trace} \ R(t, H) = \text{trace} \ HQH^T.$$

Markov Stability can be used to evaluate the quality of a particular partition found by whichever means or, alternatively, we can use it as an objective function to be maximised over the space of all possible partitions at each value of the Markov time, $t$. This latter approach is followed in the examples below to find good communities with high Markov Stability.

For Markov time $t$, we maximise Markov Stability \cite{6} over the space of all possible network partitions $H$. This optimisation is NP-complete,\cite{32} and
so we use the heuristic greedy Louvain algorithm\textsuperscript{33} which has been shown to provide an efficient optimisation of this function both in benchmarks and in real-life examples. Note that although the Louvain algorithm is formulated for symmetric matrices, and the matrix $Q$ is not symmetric, we can optimise the directed Markov Stability objective function (6) by exploiting the fact that $\text{trace}(H^TQH) = \frac{1}{2}\text{trace}(H^T(Q + Q^T)H)$ and optimising this symmetrised function. The greedy Louvain algorithm is deterministic, but the outcome of the optimisation is dependent on the random initialisation seed. We therefore run the algorithm 100 times with different random seeds and choose the partition with the highest Markov Stability. We also record the variability in the ensemble of optimised solutions by computing the average normalised variation of information (VI), a measure of the distance between two partitions\textsuperscript{34}, between all pairs in the ensemble of 100 optimised partitions. A low VI signifies that there is little difference between the obtained partitions, and we use this as an indication that the community structure of the network at this scale is robust.

By optimising the Markov Stability $r(t,H)$ across a range of times $t$ (usually spanning several orders of magnitude), we obtain a sequence of progressively coarser partitions. We do not expect to find relevant structure at all scales. Meaningful communities are chosen according to a double measure of robustness: they should be optimal, according to their Markov Stability, over long expanses of time, making them robust across time scales; they should have low values of their VI, making them robust solutions to the optimisation problem.

3. Finding flow roles in directed networks using Role-Based Similarity

In the above discussion, Markov Stability was introduced as a method for identifying groups of nodes based on the flow of information retained within them over time. We now introduce another graph-theoretical method that uses flow for a different purpose; namely, to identify instead groups of individuals who, although not necessarily close within the Twitter network, have similar patterns of incoming and outgoing flows at all scales. Such groups can be identified as flow roles in the network (e.g., source-like or sink-like in the simplest cases), and can be found through a node similarity measure called role-based similarity (RBS)\textsuperscript{21,35} Once this RBS node similarity is obtained, we transform it into role-based similarity graph through the use of the relaxed minimum spanning tree (RMST) algorithm. The
3.1. **Role-based similarity**

Each node in the network is assigned a ‘profile vector’ that encodes the pattern of in-flows and out-flows passing through that node, computed from the numbers of incoming and outgoing paths of all lengths from that node. The cosine similarity between the profile vectors of all nodes is then computed to obtain the RBS similarity matrix. Two nodes are similar if they have similar in- and out-patterns of network flow through them for all path lengths.

Formally, consider a graph with $N$ nodes and adjacency matrix $A \neq A^T$. The profile vector for a node is a $1 \times 2K_{\text{max}}$ vector: the first $K_{\text{max}}$ entries describe the number of paths of length 1 to $K_{\text{max}} < N - 1$ which begin at that node, and the second $K_{\text{max}}$ entries give the number of paths which end at that node (scaled by a tunable constant). These vectors can be computed straightforwardly by observing that the entries of successive powers of the adjacency matrix give the number of paths of increasing lengths between any two nodes (i.e. $(A^k)_{ij}$ is the number of paths of length $k$ between nodes $i$ and $j$). The profile vectors are then the row vectors of the $N \times 2K_{\text{max}}$ matrix given by

$$X(\alpha) = \begin{bmatrix} \ldots \left(\frac{\alpha}{\lambda_1} A^T\right)^k 1 \ldots \left(\frac{\alpha}{\lambda_1} A\right)^k 1 \ldots \end{bmatrix},$$

where $\alpha \in (0, 1)$ and $\lambda_1$ is the largest eigenvalue of $A$. The choice of $\alpha$ changes the rate of convergence of the terms $((\alpha/\lambda_1)A^T)^k$, and hence controls the relative influence of the large-scale structure of the graph. For small $\alpha$, the RBS similarity is based mostly on short paths, i.e., local neighbourhoods. For instance, in the limit $\alpha \to 0$ only $d_{\text{in}}$ and $d_{\text{out}}$ are taken into account. Conversely, using larger values of $\alpha$ leads to profile vectors which include more global information from the graph.

The RBS similarity of two nodes $i$ and $j$ is then given by the cosine distance between their profile vectors

$$Y_{ij} = \frac{x_i x_j^T}{\|x_i\|\|x_j\|},$$

where $x_i$ and $x_j$ are the $i$th and $j$th rows of $X$. 
3.2. Relaxed minimum spanning tree

The similarity matrix $Y$ defined by (8) can be thought of as a complete, weighted graph on the nodes, with edges between every pair of nodes weighted by the cosine similarity of their respective profile vectors. Note however that the matrix $Y$ also represents the similarity between transient (forward and backward) time courses of the linear dynamics on the network. Given the intrinsic continuity of this dynamic representation, we obtain a sparser projection through the use of the relaxed minimum spanning tree (RMST) algorithm, a method to obtain a graph-theoretical projection that captures the underlying continuous geometry of the vectors being considered—here, the points are the profile vectors, which lie in a $2K_{\text{max}}$-dimensional space.

The algorithm proceeds as follows: the minimum spanning tree (MST) of the complete graph $Y$ is calculated. For each pair of points $i$ and $j$ the edge $Y_{ij}$ is then added to the graph if it is not too much larger than than the largest edge weight in the MST path between $i$ and $j$. Formally the edges in the RMST are given by

$$\text{RMST}_{ij} = \begin{cases} 
1 & \text{if } y_{ij} < m\text{link}_{ij} + \gamma(d_{i}^{k} + d_{j}^{k}), \\
0 & \text{otherwise},
\end{cases} \quad (9)$$

where $m\text{link}_{ij}$ is the largest edge weight in the MST path between nodes $i$ and $j$, $d_{i}^{k}$ is the distance from node $i$ to its $k$th nearest neighbour and $\gamma$ is a positive parameter (here we have used $k = 1$ and $\gamma = 0.5$). The term $\gamma d_{i}^{k}$ is a measure of the local density around every point.

4. Twitter data of the care.data debate: follower and retweet networks

The networks analysed here are obtained from a set of tweets relating to the care.data debate. All tweets sent between 1 December 2013 and 27 March 2014 containing the text “care.data”, “caredata” or “care data” were obtained from the provider Gnip. There were 36,745 tweets from 10,031 accounts. The data included the tweeters screen name, the tweet text and the date and time the tweet was sent. Lists of followers of each user in the data set were obtained using the Twitter API (this was carried out in April 2015).

\[^{a}\text{www.gnip.com}\]
We then constructed two directed networks (Fig. 1): (a) the usual network of followers (‘who follows whom’) amongst the users who appeared in the data set; and (b) the weighted network of retweets (‘who has retweeted whom and how much’). We study the largest connected components of these two networks: the follower network has a single connected component with \( N = 10,031 \) users (nodes) and \( E = 472,428 \) edges, corresponding to declared following; the largest connected component of the retweet network has \( N = 7303 \) nodes and \( E = 14542 \) edges, corresponding to actual retweet activity during this period. The follower network (a) is analysed in Sections 5.1–5.5, whereas the retweet network (b) is studied in Section 5.6.

Using directed Markov Stability, we identify communities in both networks. The communities of users obtained in the network of followers are called interest communities, whereas the communities found in the retweet network are referred to as conversation communities. To provide a visual representation of the common interests within interest communities, and the topics of discussion within conversation communities, we have used the profile text (self-descriptions) of the users and the text of their tweets, usually in the form of word clouds. It is important to remark that the text of the tweets and self-descriptions is only used \textit{a posteriori} to illustrate our findings. The follower network is also used to identify roles in the network using the RBS-RMST algorithm, as described in Section 3.

5. Results

5.1. Identification of interest communities in the follower network

By applying the flow-based community detection method Markov Stability to the directed graph of follower relations we identify interest communities: groups of users between whom information, interest and influence is
Fig. 2. Interest communities identified by Markov Stability in the follower network. The word clouds show the most commonly appearing words in the personal profiles of the users in the different communities.

propagated. As seen in our previous studies of Twitter networks, the directionality of the edges is important for capturing this information flow; communities in undirected networks are diffuse and blurred compared to those in the equivalent directed network. Our computations of the directed Markov Stability across times shows a long plateau between Markov times 4.3 and 6.1 accompanied by a low variation of information, indicating that the 13-way partition found during this period is robust. Below, we concentrate on this partition although other levels of resolution can provide different information.

The 13-way partition is composed of four large communities (comprising 99.16% of the users) and nine minor communities, which were not considered further. As shown in Figure 2 our *a posteriori* analysis of the most frequently appearing words in the users’ personal profiles (self-descriptions) reveals that the three major interest communities correspond to: healthcare professionals, politicians and political activists, and self-confessed ‘data geeks’ and media types. The most common words in the self-descriptions of the healthcare community were ‘health’, ‘nhs’, and ‘care’; the politics community featured words such as ‘labour’, ‘politics’, and ‘people’; and the media/data community users used words such as ‘data’, ‘geek’, and
‘science’. The care.data programme is a healthcare scheme, but the issues surrounding its implementation concerned the proper use of personal data and related security and privacy issues. The fourth largest community presented a mixed set of words including ‘healthcare’/‘health’/‘medical’, but also ‘data’, ‘technology’ or ‘business’. Interestingly, a closer analysis of the users of this community revealed that this group was mainly US-based, and only collaterally participating in the debate due to interest both in data issues and the relevance of NHS reforms to healthcare reforms in the US. Our analysis thus confirms that the nature of the debate is reflected in the different interests of those Twitter users who actively engaged with the debate.

5.2. **Audience of the interest communities**

Although Twitter is an open platform, in which anybody is able to create a free account and participate, the analysis of personal profiles suggests that users who engaged in the care.data debate had pre-existing personal interest in the issues being discussed (healthcare, privacy and data security, politics etc.). To understand the global reach of the debate outside the network analysed, we collected the follower list of each user in our network, i.e., all the Twitter users who could have seen a tweet or retweet related to care.data. The number of unique followers was 9.6 million - nearly as many as could be reached by a prime-time Saturday night television advert - demonstrating the clear potential of Twitter as a medium for policy communications (although it is likely that some of these users are ‘fake’ accounts).

Our analysis reveals relatively little overlap between the outside followers of the different communities: 70% of followers of the politics group, 76% of followers of the media/data group, 54% of followers of the healthcare group, and 64.4% of the US group followed only people in that particular interest community (Fig. 3). To ensure that a wide and diverse audience is reached, it is therefore important for policy makers to understand and engage with the different communities in the debate.

Table 1 shows the users within each community with the largest number of followers. Users in the media/data community with large numbers of followers include the satirist Armando Iannucci (@aiannucci); the physician and popular science writer Ben Goldacre (@bengoldacre); and the blogger and digital rights activist Cory Doctorow (@doctorow). Users in the healthcare community with a large reach include the British Medical
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Fig. 3. Total unique followers of users in each of the four main interest communities.

| Media/Data | Politics | Healthcare |
|------------|----------|------------|
| Aiannucci  | 42282    | 596380     | Dr_Squid_001* (82%) 226264 |
| bengoldacre| 378681   | davidicke  | bmj_latest  161007 |
| doctorow  | 359954   | walkon_crafters* (85%) 117813 NHSChoices 159852 |
| digiphile | 236273   | NHAparty  | 64416 mencap_charity 84889 |
| WiredUK   | 224780   | labourpress | 56264 TheStrokeAssoc 67491 |
| cybersdefensemag | 199768 | OccupyLondon  56773 NHSEngland  65673 |
| pzmyers   | 163682   | IndyVoices | 52191 TheRIU  60561 |
| tom_watson| 161073   | politicalhome | 56554 TheBMA  47059 |
| arasbridger| 151213  | sabi_anaa | 46996 GdnHealthcare  44887 |

* Users in italics have > 80% estimated fake followers (percentage in parenthesis)

Journal (@bmj_latest), the English NHS (@NHSChoices), and the Department of Health (@DHGovuk). The three users with the most followers in the politics community were slightly unusual: a user posting mainly photos of art (@Asamsakti), the controversial conspiracy theorist David Icke (@davidicke), and a support group for amputees (@walkon_crafters). However, using an online tool[^1] we found that 81% of followers of @Asamsakti and 85% of the followers of @walkon_crafters are estimated to be ‘fake’ user accounts. Less surprising were the official accounts for the political party the National Health Action party (@NHAparty), the Labour Press Team (@labourpress), and the anti-capitalist protest group Occupy London (@OccupyLondon).

[^1]: [www.twitteraudit.com](http://www.twitteraudit.com)
5.3. Sentiment analysis of tweets

To determine the sentiment of the discussion and identify some of the topics of discussion, we manually analysed a sample of 250 tweets from the dataset (Table 2). Very few of the tweets were classified as positive (3-5%), the rest being neutral or negative. This is characteristic of how Twitter is used—spikes in tweet activity around a particular event tend to be of a negative nature. Interestingly, however, the proportion of tweets from users in the healthcare community which were classified as negative was lower than in the politics and media/data communities.

There were also differences in the content of the negative tweets between the three interest communities. We divided concerns into three distinct classes:

1. Implementation. Concerns regarding information provision, the opt-out process, and communication with the public.
2. Scheme concept. Concerns about privacy, sharing of personal data, and the use/sale of the data.
3. Execution. Concerns around security, effectiveness of pseudonymisation, and cyber attacks.

While all three communities were predominantly negative about the care.data scheme, each focused on different arguments. The politic community mainly discussed the scheme concept of sharing personal data, as well as the security concerns that are associated with it. The healthcare and media/data communities on the other hand were primarily concerned about the implementation of the care.data project, concentrating on the contested opt-out arrangement and perceived lack of communication to the public.

5.4. Bridgeness between communities

The communities identified in the follower network are regions where a dynamical process is likely to become trapped, so information flows less readily between these communities than within them. This suggests that relatively few links could act as a ‘bridge’ between communities and could be effective at propagating the flow from one to another. An example of such a connection would link one user who is following influential individuals in one community and another who is being followed by many people in another community (Fig. 4). To identify the ‘bridges’ from community $C_1$ to community $C_2$, we calculate the shortest paths between all pairs of
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Table 2. Sentiment and content analysis of a random sample of 250 tweets.

| Tweet sentiment | Healthcare | Politics | Media/Data |
|-----------------|------------|----------|------------|
| Positive        | 5%         | 4%       | 3%         |
| Negative        | 58%        | 75%      | 62%        |
| Neutral         | 37%        | 21%      | 35%        |

| Major concerns       | Healthcare | Politics | Media/Data |
|----------------------|------------|----------|------------|
| Implementation¹      | 65%        | 28%      | 54%        |
| Scheme concept²      | 28%        | 43%      | 35%        |
| Execution³           | 7%         | 29%      | 11%        |

¹ information provision, the opt-out process, communication to the public
² privacy, sharing of personal data, use/selling of the dataset
³ security concerns, re-identification, cyber attacks

nodes \((i, j)\), where \(i \in C_2\) and \(j \in C_1\). Note that the flow of information is in the opposite direction to that of the edges: if there is an edge from node \(i\) to node \(j\), then content produced by user \(j\) is consumed by user \(i\). The bridgeness (centrality) of an edge is then defined as the proportion of shortest paths which pass through that edge - this is equivalent to the classic betweenness centrality measure, but now only shortest paths between specific subgroups of the nodes are considered. Such information could be useful for policy-makers who find they have more success in engaging users in community \(C_1\) than in \(C_2\) - since they will be able to target those users in \(C_1\) who are most able to propagate that information on to \(C_2\).

As an illustration of the type of information that can be extracted, we have considered the bridging links with the highest bridgeness centrality between the three largest communities (Fig. 4). (A more nuanced view can be obtained by considering a longer list of bridges and their profiles, see Table 3). The highest bridgeness centrality for flow from the politics community to the healthcare community is the link from Roy Lilley (@RoyLilley) to the National Health Action party (@NHAparty). Roy Lilley is followed by 44.4% of users in the healthcare community, and the NHA party is following 41.0% of users in the politics community. The highest bridgeness centrality for flow in the opposite direction (from the healthcare community to politics) is the link from the NHA party to NHS healthcare professional Helen Bevan (@helenbevan). The NHA party is being followed by 53.2% of the politics community and Helen Bevan is following 19.1% of the healthcare community. The partial asymmetry here is interesting: within the politics community, the NHA party has a large number of followers (53.2%) and a large number of users it follows (41.0%), meaning it
Fig. 4. Bridgeness. a) To identify the users important for information flow between two communities, we compute the shortest paths for all pairs of nodes \((i, j)\) where \(j \in C_1\), \(i \in C_2\) and identify the between-community edges which feature in these shortest paths most often. Shortest paths are likely to go through UserA (who is being followed by many users in \(C_2\)) and UserB (who is following many people in \(C_1\)). b) Links with highest bridgeness centrality between interest communities - note that the flow of information is in the opposite direction to that of the edges.

is able to act as both a broadcaster of information to this community and a receiver of information from it. In contrast, Roy Lilley is followed by a large proportion of people in the healthcare community (44.4%) but follows relatively few (3.4%); he is therefore more likely to act as a broadcaster of information to the community. Helen Bevan follows a larger proportion of the healthcare community (19.6%), and is therefore exposed to a larger amount of the content generated by its users.

A similar asymmetric pattern is observed for information flow between the healthcare and media/data communities, and between the media/data and politics communities. The highest bridgeness centrality for healthcare to media/data is via the link from Ben Goldacre (@bengoldacre) to Julia Cox (@JuliaHCox), whereas the highest bridgeness centrality for flow in the opposite direction is via the link between the Mencap charity (@mencap_charity) and the Open Rights Group (@OpenRightsGroup). Flow from politics to media/data is via the link between Armando Iannucci and the NHA party, whereas flow from media/data to politics is via the link between the NHA party and the software company figshare (@figshare).

The asymmetry observed in the bridgeness centralities reinforces the
Table 3. The top 5 bridging edges in the boundaries across interest communities ranked according to their bridgeness ratio (BR). The bridgeness ratio of an edge is the number of shortest paths from $C_1$ to $C_2$ which pass along that edge divided by the expected number of paths to pass along any edge at that boundary. A high BR means that a disproportionally large number of shortest paths pass through this edge.

Due to the asymmetry of the information flow from followed to follower, the relevant edges are different depending on the direction in which the boundary is crossed.

| Politics → Media/Data | BR | Politics → Healthcare | BR | Media/Data → Healthcare | BR |
|-----------------------|----|-----------------------|----|-------------------------|----|
| @NHAparty → @figshare | 59.9 | @NHAparty → @helenbevan | 277.8 | @bengoldacre → @JuliaHCox | 62.9 |
| @NHAparty → @PennyLansom | 52.5 | @NHAparty → @RichardGP | 200.6 | @bengoldacre → @WelchAdvisors | 48.8 |
| @NHAparty → @PentaxUK | 52.2 | @NHAparty → @HealthCare | 91.3 | @bengoldacre → @HealthcareUK | 44.0 |
| @NHAparty → @uknhs | 43.1 | @NHAparty → @HSMedical | 82.3 | @bengoldacre → @AzeemMajeed | 40.8 |
| @ScottishGp → @bryankirwan | 41.6 | @NHAparty → @HSMCR | 79.8 | @bengoldacre → @Sam_just | 37.1 |

| Media/Data → Politics | BR | Healthcare → Politics | BR | Healthcare → Media/Data | BR |
|-----------------------|----|-----------------------|----|-------------------------|----|
| @Aiannucci → @NHAparty | 208.9 | @RoyLilley → @NHAparty | 203.8 | @OpenRightsGroup | 35.7 |
| @jwolff → @SteveBurnsJohn | 51.8 | @ManchesterCCGs → @KayFSheldon | 108.5 | @Psychemedia | 32.2 |
| @bengoldacre | 50.8 | @simplemum | 91.8 | @bmj_latest | 30.5 |
| @AlexRidings → @NHAparty | 46.1 | @asthma_uk | 48.1 | @Haloes1 | 30.3 |
| @bengoldacre | 45.9 | @Twitter | 48.3 | @StAnnes | 27.3 |

notion that directionality is crucial for understanding patterns of information flow through the network. It also suggests that, depending on the users someone is following and being followed by, individuals might play different roles in propagating the flow of information through the network. We explore this idea in more detail in the following section.

### 5.5. Identifying roles in the follower network

To identify the different roles played by users in propagating the flow of information via the Twitter social graph, we constructed the RBS-RMST similarity graph for the follower network. We then used Markov Stability on this similarity graph to identify groups of nodes with similar in-flow and out-flow patterns. We find a robust partition of the similarity graph into 6 groups, which correspond to 6 distinct roles for the Twitter users according to their flow patterns (Fig. 5a). The meaning of the 6 roles identified can be understood by considering the aggregated in- and out-flows in the social graph for each of the roles; by computing the in- and out-degree for each role; and by obtaining the proportion of their friends who lie in a different interest community. All of these characterisations are presented in Fig. 5b-d.

The combined information from all these measures allows us to describe the identified roles as:

1. **Leaders**: users with higher in-degree (number of followers) than out-
Fig. 5. Role communities in the role-based similarity graph. a) Role-based similarity graph obtained using the RBS-RMST algorithm, there are 6 robust communities corresponding to different user roles. b) The original follower network coarse-grained into role communities, the arrows are proportional in size to the number of users in one role community who follow users in the other role community. c) average in-degree and out-degree of users in the 6 role communities. d) Kernel density estimates for the distributions of the proportion of a user’s friends lying outside their own interest community. e) Cumulative distribution of retweets for the different role communities.

degree. Users in this group tend to follow few people, mainly in the mediator group.

(2) Mediators: users with roughly the same in-degree and out-degree who are both following and being followed by users in all other groups.

(3) Listeners: users with few followers, and who are following a small number of people from primarily the ‘Leader’ group.

(4) Diversified listeners: users with few followers, but who are following a larger and more diverse group of users than the ‘Listener’ category.

(5) Peripheral followers: users who are following a very small number of other users and are being followed by no-one.

(6) Peripheral followed: users who are being followed by a small number of users but are following no-one.
The users with the largest number of followers in the ‘Leader’ role are the physician and science writer Ben Goldacre; former Chair of the Council of the Royal College of General Practitioners Clare Gerada (@clareregp); and the account of the Department of Health. In the ‘Mediator’ role, the NHA party, the Joseph Rowntree Foundation (@jrf_uk), and Care Quality Commision board member Kay Sheldon (@KayFSeldon) have the largest number of followers.

We calculated the proportion of each user’s friends (users they are following) who are in a different interest community from themselves (as calculated in Section 5.1) for each of the different roles (Fig. 5d). The diversified listeners have the greatest proportion of friends outside their own interest community, which confirms that these users are following a broad range of other accounts involved in the care.data debate. The mediators and leaders also tend to follow a significant number of people outside their own interest community. The listeners and peripheral listeners follow predominantly others within the same interest community, suggesting that their involvement or interest was focused on one particular aspect of the debate.

To understand how the different roles identified in the follower network translate into actual participation in the care.date debate we calculated the distributions of retweets for each of the role communities (Fig. 5e). There is a clear separation between the ‘Leader’ category, which garners the most re-tweets, and the follower categories ‘Listener’ and ‘Diversified Listener’, which are rarely retweeted, with the ‘Mediator’ category lying in-between but closer to the ‘Leader’ group. These results suggest that identifying users who have ‘Leader’ and ‘Mediator’ roles in follower networks can predict those users who are likely to have greatest influence in the debate. We now explore the structure of the retweet network obtained from the collected tweet corpus.

5.6. Conversation communities in the retweet network

The Twitter social graph (i.e., the follower network studied above) encodes the possibility of information flow through Twitter—tweets from a user you are following will appear on your timeline and you have the opportunity to retweet them or send a related tweet. Of course, most people cannot and do not engage actively with all information they are exposed to. Since we have the set of all tweets concerning care.data, we are able to explore the actual flow of information on this specific topic. To allow us to understand the issues being discussed, and the groups of people who are actively engaging
with each other through Twitter, we have therefore analysed the network of retweets (‘who retweets whom and how much’) using our community detection framework to find conversation communities. We then interpret the results through an \textit{a posteriori} summary of the text of the tweets in the obtained groups.

Applying Markov Stability, we identify a robust partition of the retweet network into \textit{8 conversation communities} (Fig. 6). Table 4 shows how participants within each conversation community are split between the three largest interest communities (healthcare, media/data, politics). The conversation communities contain an uneven split of users from the interest communities: except conversations 5 and 8, all conversations are dominated by users from a particular interest community. This result confirms that in the care.data debate there is a greater flow of information between users with similar interests, and this implies that interest communities (identified from the network of follower relations) provide a good indication of how information is likely to flow through the Twitter network.
Table 4. Mix of users in the 8 conversation communities according to the 3 main interest communities. The + and − signs indicate whether the observed number of users is above or below expectation. All conversation communities (except Conversation 4) are significant ($p < 0.001^{(***)}$) according to a chi-square statistic calculated for each row independently.

| Conversation | Politics | Media/Data | Healthcare |
|--------------|----------|------------|------------|
| 1            | 201(−)   | 113(−)     | 808(+)     |
| 2            | 427(−)   | 778(+)     | 334(−)     |
| 3            | 834(+)   | 532(−)     | 290(−)     |
| 4            | 0(−)     | 2(+)       | 0(−)       |
| 5            | 65(+)    | 54(+)      | 1(−)       |
| 6            | 29(−)    | 261(+)     | 16(−)      |
| 7            | 66(−)    | 15(−)      | 161(+)     |
| 8            | 754(+)   | 632(+)     | 311(−)     |

To identify the topics being discussed within the different conversations, we extracted the text of the tweets and retweets sent by users within each group and produced word clouds with the most frequent words used in those conversations (Fig. 6). Conversation 1 centred primarily around healthcare professionals discussing the impact of the scheme on patients, containing words such as ‘patient’, ‘public’, and ‘people’. The media and data tweeters in conversation 2 were more opinionated, using words like ‘mess’, ‘wrong’, and ‘sorry’. In conversation 3, political activists discussed privacy issues such as the ‘opt out arrangement, the selling (‘sold) of ‘records’ to ‘insurance’ companies, and the involvement of the controversial digital services company Atos. Conversation 6 was dominated by data geeks, who discussed ‘medical records and privacy issues. Finally, conversation 8 brought together users from both the healthcare and data communities in a more general discussion.

6. Conclusion

By applying the multiscale flow-based community detection method Markov Stability to follower networks of Twitter users, we have identified separate participating groups in the debate concerning the healthcare programme care.data. We have shown that users within these groups share similar interests, and that the audience of Twitter users outside the network (i.e. those who did not participate in discussion of care.data, but follow someone who did) are distinct for the different communities. By analysing the retweet network, we have identified specific topics being dis-
cussed in different conversation communities. Furthermore, by comparing the communities found in the follower and retweet networks, we have shown that the actual flow of information (in the form of retweets) is heavily influenced by the network of follower relations. Using role-based similarity, we have classified the users in the care-data debate according to the role they play in propagating information across the network. The information uncovered by these methods could be of great value to policy makers, who, in order to target the largest possible audience, need to understand the different communities and the different roles played by the individuals within them.

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