Nano-spectroscopy of excitons in atomically thin transition metal dichalcogenides

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Excitons play a dominant role in the optoelectronic properties of atomically thin van der Waals (vdW) semiconductors. These excitons are amenable to on-demand engineering with diverse control knobs, including dielectric screening, interlayer hybridization, and moiré potentials. However, external stimuli frequently yield heterogeneous excitonic responses at the nano- and meso-scales, making their spatial characterization with conventional diffraction-limited optics a formidable task. Here, we use a scattering-type scanning near-field optical microscope (s-SNOM) to acquire exciton spectra in atomically thin transition metal dichalcogenide microcrystals with previously unattainable 20 nm resolution. Our nano-optical data revealed material- and stacking-dependent exciton spectra of MoSe₂, WSe₂, and their heterostructures. Furthermore, we extracted the complex dielectric function of these prototypical vdW semiconductors. s-SNOM hyperspectral images uncovered how the dielectric screening modifies excitons at length scales as short as few nanometers. This work paves the way towards understanding and manipulation of excitons in atomically thin layers at the nanoscale.
Excitons, bound electron–hole pairs, govern the optical properties of two-dimensional transition metal dichalcogenides (TMDs) over near-infrared (IR) and visible frequencies due to their large binding energy and prominent oscillator strength. Notably, all excitonic parameters in TMDs, including their resonance energies as well as both radiative and non-radiative lifetimes, can be manipulated on demand. Relevant control mechanisms include electric and magnetic fields, heterostructuring, moiré superlattice potentials, local strain, ultrafast optical excitation, dielectric screening, and others. The vast majority of experimental studies of excitonic phenomena in TMDs have been carried out by far-field optical methods with wavelength-limited spatial resolution. Nanoscale probes of the engineered excitonic electrodynamics are required to explore heterogeneous features. Nano-probe experiments reported here have the potential to map out the spatial evolution of exciton resonance energies in structures with (spatially) controlled dielectric screening and interlayer hybridization. In addition, nano-spectroscopy can document the potential role of extrinsic factors, such as defects and impurities, especially wrinkles and contaminations common in atomically layered nanostructures. Finally, applications of TMDs in nanophotonics and optoelectronics will benefit from characterization of excitons in nanodevices with sub-diffractional feature sizes that we demonstrated in our study.

A variety of scanning probe optical methods are in general suitable for the nanoscale characterization of the excitonic properties. Specifically, tip-enhanced photoluminescence (TEPL) studies have uncovered aspects of nanoscale excited state recombination in TMDs. Complementary to the TEPL, absorption spectra encode not only the exciton resonance energy but also the oscillator strength and damping rate, offering additional detailed inquiry into the excitonic response. In principle, local absorption spectra acquired by scanning-type scanning near-field optical microscopy (s-SNOM) allow one to obtain the complex dielectric function, \( \varepsilon(\omega) = \varepsilon_r(\omega) + i\varepsilon_i(\omega) \), and make it possible to probe the engineered excitons at the nanoscale. This latter capability has been extensively used to study plasmons and phonons in other classes of van der Waals (vdW) materials, as well as interlayer hybridization in a multi-layer WSe\(_2\) crystal.

Here, we coupled an ultra-stable and tunable continuous-wave Ti:sapphire laser (M squared) to a commercial s-SNOM (Neaspec GmbH) and investigated the nanoscale excitonic spectra in monolayer TMD semiconductors and heterostructures. The exciton resonance energy, radiative lifetime, and the damping rate in these samples is 1.50–1.75 eV, which covers the 1s exciton resonance energies of WSe\(_2\) and MoSe\(_2\) monolayers (see inset in Fig. 1b). In this energy range, the near-field signal from h-BN is frequency-independent and can be utilized as a reference for spectroscopic data of TMD materials. The normalized near-field amplitude and phase at the \( n \)-th harmonic and energies \( \omega \) are denoted by \( s_n(\omega)/s_n(h \rightarrow \text{BN}) \) and \( \varphi_n(\omega) - \varphi_n(h \rightarrow \text{BN}) \), respectively. A combination of our ultra-stable laser and scanner system allowed us to demodulate the scattering signal at the fifth harmonic of the tapping amplitude; high harmonic data is imperative for obtaining genuine near-field contrast devoid of far-field artifacts.

To display the excitonic responses in the near field, in Fig. 1c–e we show representative s-SNOM images for a sample with monolayers of MoSe\(_2\) and WSe\(_2\), MoSe\(_2\)/WSe\(_2\) heterobilayer, and unobscured h-BN all in the same field of view (FOV) of our apparatus. An AFM topographic image is shown in Fig. 1c, where a substantial height variation from left to right is prompted by a terrace in the underlying h-BN substrate. Nevertheless, regions of monolayer, bilayer, and multilayer TMDs can be readily identified by their topographic height. Our layer thickness assignment is further confirmed by the second harmonic generation (SHG) data (see Supplementary Figs. 2 and 3). The co-located images of topography (Fig. 1c), near-field scattering amplitude (Fig. 1d), and phase (Fig. 1e) are all acquired simultaneously. The amplitude image (Fig. 1d) reveals nearly uniform signals collected within terraces demarcated by boundaries between the terraces. We acquired images in Fig. 1d, e by setting the excitation photon energy at 1.68 eV. At this energy, a strong phase contrast between the WSe\(_2\) monolayer and h-BN substrate is observed (Fig. 1e). On the contrary, no discriminable phase contrast is found for the MoSe\(_2\) monolayer. The observation is readily understood as the near-field phase is related to the absorption. The different excitonic absorption characteristics of the TMDs can give rise to phase contrast. According to our hyperspectral data in Fig. 2, the photon energy of 1.68 eV is close to the exciton resonance in WSe\(_2\) monolayer and does not overlap with the excitonic band of MoSe\(_2\) centered at 1.58 eV. Our data reveal that the prominent nano-optical contrast in Fig. 1 is rooted in the local excitonic response of TMD monolayers. It should be noted that the contributions of thermal effect and charge effect to the near-field contrast can be ruled out by the high harmonic demodulation as also evident in the near-field spectra shown in following sections.

Near-field nano-spectroscopy of excitons in WSe\(_2\) monolayer. For quantitative analysis of the WSe\(_2\) monolayer excitonic response, we carried out raster-scanned nano-imaging while
varying the photon energy with a step size of ~10 meV. We have simultaneously collected topographic and near-field maps at each energy over the same FOV marked by the dashed rectangle in Fig. 1d. The topography image and height profile are shown in Supplementary Fig. 3. The unobscured h-BN in the upper left corner of Fig. 2 is used as a reference for normalization purposes. Representative maps of the normalized fifth-harmonic amplitude $s_5(\omega)$ and phase $\phi_5(\omega)$ are shown in Fig. 2a, b, respectively. In these images, both the amplitude and phase signals in WSe$_2$ monolayers vary systematically as a function of excitation energy. In particular, the phase images display a prominent contrast centered around 1.66 eV. Notably, we witness a highly uniform response within regions occupied by each of the TMD materials in Fig. 2. All the boundaries and some terraces are in a deeply sub-diffraction regime. Nevertheless, these features can be clearly discriminated in our s-SNOM images. To quantify the excitonic response, we start our analysis by averaging the near-field signals over the entire region occupied by WSe$_2$ monolayer at each probing frequency. The averaging process will facilitate a more faithful determination of dielectrics function, which will be discussed later. The net result is that each data point in spectra plotted in Fig. 2c, d is representative of the entire region imaged at the corresponding energy in Fig. 2a, b. The spectra derived from images show prominent resonance characteristics: the amplitude signal reveals a dispersive behavior around 1.66 eV, whereas the phase signal exhibits a peak centered at the same energy.

We modeled experimental near-field spectra of WSe$_2$ in Fig. 2 with the Lorentzian form of the dielectric function:

$$\varepsilon(\omega) = \varepsilon_\infty - \frac{C}{\omega_0^2 - \omega^2 + i\omega \gamma_r}$$

where $\varepsilon_\infty$ is the high-frequency permittivity limit and originates from all transitions with frequencies beyond the spectral range investigated here, $C$ is the speed of light in vacuum, $\omega_0$ is the exciton resonance energy, $\gamma_r$ is the monolayer thickness, $\gamma_r$, $\gamma_n$, $\gamma_d$ are radiative, non-radiative, and dephasing decay rates, respectively. The oscillator strength of the Lorentzian in Eq. 1 is related to the radiative rate $\gamma_r$. We choose the point dipole model to interpret the data as it is well documented to capture the response of atomically thin samples laid on thick substrates. As shown in Fig. 2c, d, the point dipole model with Eq. 1 as the input dielectric function provides an adequate fit to the data (see SOM for details on fitting).

Now we analyze the parameters inferred from the fitting procedure (Table 1). The obtained dielectric function is plotted in Fig. 2e. The radiative rate for monolayer WSe$_2$ is 1.4 meV, which corresponds to the radiative lifetime $\tau_0 = \frac{\hbar}{\gamma_r}$ of ~233 fs. This latter finding is consistent with the first principles theoretical values and experimental results derived from the ultrafast exciton 1s-2p transition, which reveal 150 fs radiative lifetime in WSe$_2$ monolayers. The shorter radiative lifetime compared to that of conventional semiconductors stems from the exceptionally...
large exciton oscillator strength in two-dimensional TMDs, evidenced by the high optical absorption in monolayer. We obtained the damping rate $\frac{\hbar}{2} + \gamma_d = 15$ meV. We remark that this substantial damping at room temperature inhibits the real dielectric function from crossing zero, and thus the exciton polariton regime cannot be reached. Recently, reflection measurements at cryogenic temperature demonstrated the negative real dielectric function in the vicinity of the excitonic line. Therefore, by reducing the damping rate, for example, through experiments conducted at cryogenic temperature, it may become possible to access the exciton polaritons in monolayer TMDs. So far, all experiments on exciton polaritons in TMDs conducted at ambient required integration of the active semiconductor in various forms of photonic cavities. A notable exception is an observation of the excited state Rydberg exciton polaritons demonstrated in pump-probe experiments for multilayer WSe$_2$ at room temperature.

Next, we comment on the contributions of bright and dark excitons to the s-SNOM spectra. These two types of excitonic species result from the spin splitting of the conduction band edge and they obey different optical selection rules. In TMD literature, excitons that can be excited by light with polarization in the sample plane, as in normal incidence experiments, are referred to as bright excitons. Excitons that can be activated only
when light polarization is perpendicular to the sample plane, are referred to as dark excitons. Dark excitons can be visualized using TEPL for TMD samples on metallic substrates because the electric field strength perpendicular to the sample surface is drastically enhanced. In contrast, the s-SNOM signal for atomically thin TMDs is governed by the in-plane dielectric function, which arises from bright excitons (see SOM). To experimentally confirm the dominant role of bright excitons in our data, we compared the bright exciton resonance energy obtained from far-field PL spectra on the same sample with the resonance energy in our s-SNOM spectra. The bright exciton resonance energy from PL (see Supplementary Fig. 4) is about 1.66 eV, in close agreement with s-SNOM data. We, therefore, conclude that bright excitons dominate the s-SNOM response of monolayer and few-layer TMD crystals.

As discussed above, the s-SNOM spectra are determined by the dielectric function of the materials; whereas TEPL is determined by both the exciton population and the transition rate, which gives rise to inhomogeneity of the TEPL. Here, to probe the intrinsic properties of TMDs, the samples are exfoliated from the high-quality crystals grown by the self-flux method and fabricated by the contamination-free stacking method (details in “Methods”). The resulting high-quality sample possesses nearly uniform dielectric function, thereby exhibiting a nearly homogenous s-SNOM signal.

Excitonic spectra of TMD monolayers. Before exploring the nanoscale response of heterostructures and multilayers, we take a closer look at the near-field response of the constituent monolayers. The spectra of the normalized amplitude and phase for MoSe2 are shown in the middle panels of Fig. 3a, b (see Supplementary Fig. 6 for complete data sets). Each data point in these spectra is attained by averaging the near-field signal over the entire MoSe2 regions. The near-field spectra for MoSe2 are akin to those of WSe2 and exhibit nearly the same resonance features, manifesting as a derivative-type lineform in the amplitude and a peak in the phase. The resonance energy observed in MoSe2 using s-SNOM (1.583 eV) is consistent with the dominant peak in PL spectra (see Supplementary Fig. 4), supporting the notion of bright excitons. The radiative rate obtained by fitting the spectra for MoSe2 is as high as 1.7 meV and is slightly larger than that of WSe2 (see Table 1). In general, the prominent radiative rates stem from the two dimensional nature of excitons in TMDs, which are tightly bound to monolayers and have a small exciton radius. Even though the spectral lineforms of excitonic lines in MoSe2 and WSe2 are nearly identical, the near-field amplitude detected for MoSe2 is considerably larger than that of WSe2 below the exciton resonance energies (top and middle panels of Fig. 3a). We also found that the magnitude of the real part of the dielectric function at energies below the exciton resonance is enhanced in MoSe2 compared to that of WSe2. This latter finding is consistent with the enhanced radiative rate in MoSe2.

MoSe2/WSe2 heterobilayers and WSe2 trilayers. Now we turn to the spectra acquired for the MoSe2/WSe2 heterostructures with the width of less than 1 μm, as shown in the s-SNOM contrast changes across the boundary between the monolayers and heterostructure. From the high-resolution images and the line profiles (Fig. 4c), one can see that the exciton resonance energy is altered over the length scale of about 20 nm, which is the spatial resolution in our experiment. We conclude that our nano-NIR/vis scans yield only the upper bound estimate of this length scale limited by the spatial resolution of our method. Our estimate is consistent with the theoretically predicted value of about 10 nm (ref. 9). Figure 4a–c displays the representative results affirming the s-SNOM contrast changes on the length scale of ~20 nm. Data in Figs. 2 and 3 uncover the abruptness of these changes both in amplitude and phase signals over the entire frequency range. The totality of the data in Figs. 2–4 attest to the nanoscale sensitivity of our approach to the dielectric function.

In addition to the dielectric screening, interlayer hybridization also plays a role in controlling the excitonic properties of van der Waals (vdW) materials, particularly in homostructures. Our nano-NIR/vis data provides an experimental access to interlayer hybridization in trilayer WSe2 exfoliated from 2H-stacked crystal. We anticipate that in these crystals neighboring layers are twisted by an angle of 60°. The amplitude and phase spectra acquired on the WSe2 trilayer are shown in Fig. 4d, e, respectively, with fitting results presented in Table 1. These data show that the exciton resonance energy decreases from 1.660 eV in WSe2 monolayer (dashed vertical line in Fig. 4e) to 1.639 eV in the trilayer (solid vertical line in Fig. 4e) to 1.639 eV in the trilayer (solid vertical

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**Methods**

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Fig. 3 Nano-spectroscopy of different types of excitons. a, b Normalized amplitude $s_h(\omega)/s_s(h-BN)$ and phase $\phi_h(\omega) - \phi_s(h-BN)$ spectra for different sample regions (data points). The near-field data is fitted by the point dipole model and Lorentz oscillators (solid curves). The vertical dashed lines are used to mark the exciton energies of WSe$_2$ and MoSe$_2$ extracted from the point dipole model. The arrows in a mark peak energies of the PL spectra (Supplementary Fig. 4). c Near-field image of the amplitude $s_h$ taken at an excitation energy of 1.52 eV. HB: heterobilayer. d, e Near-field amplitude $s_h$ and phase $\phi_h$ evolution along the line trace shown in (c). The horizontal dashed lines in d and e denote the exciton energies extracted from the point dipole model.

The indirect transitions in few-layer TMD crystals have negligible oscillator strength, and thus make only a minute contribution to the dielectric function and/or to the s-SNOM signal. Therefore, the observed redshift of the exciton resonance energy originates from direct transitions. For trilayer WSe$_2$ with a twist angle of 60°, interlayer electronic hybridization splits both conduction and valence band edges at the corner of the Brillouin zone, thus reducing the energy gap and the corresponding exciton resonance energy.$^{52,54,55}$ Therefore, the large shift observed in WSe$_2$ trilayer (21 meV) is likely to be caused by the interlayer hybridization. We note that the dielectric screening could also reduce the exciton resonance energy, but its effect is subtle (~10 meV, as demonstrated in the last section), compared to the interlayer hybridization.

In summary, the bright excitonic responses of TMD monolayers were revealed by s-SNOM hyperspectral nano-imaging. New data allowed us to extract the exciton resonance energy, oscillator strength, and damping rate all with the nanometer resolution. Nano-NIR/vis spectra and images uncovered the spatial evolution of the dielectric screening and interlayer hybridization. We obtained the upper bound of the dielectric screening length of 20 nm limited by the achieved spatial resolution of s-SNOM in this work. Our results lay the groundwork for future spatio-temporal$^{35,53}$ studies of excitonic states, including moiré excitons$^{4,56-58}$, exciton liquid$^{59}$, and exciton phase transitions$^{60}$ in a wide range of quantum materials.

Methods

Sample preparation. Monolayers of WSe$_2$, MoSe$_2$, and 30 nm thick BN were exfoliated onto SiO$_2$/Si using the standard scotch tape method. To prepare the heterostructure sample, a polydimethylsiloxane (PDMS) stamp was coated with thin polypropylene carbonate (PPC) film and subsequently attached onto a glass slide. Inverted stacking was performed on a dry transfer station with a rotatable heating stage. Thick BN and monolayers of WSe$_2$ and MoSe$_2$ were picked up subsequently, with controlled alignment. Finally, the heterostructure with PPC was peeled off from the PDMS and transferred to a clean SiO$_2$/Si substrate at 120°C. The twist angle of the heterostructure is determined by the SHG spectra from individual layers and their overlap region.

Near-field measurement. The nano-imaging was performed using a commercial s-SNOM (www.neaspec.com) based on a tapping-mode AFM. The tapping frequency and amplitude of the AFM are about 75 kHz and 50 nm, respectively. The light source is a tunable continuous laser from M Squared, including single frequency CW-532 nm module (EQUINOX), continuous-wave Ti-sapphire model with output range 700–1800 nm (SOLITIS), and frequency mixing module with tunable output range 1100–2200 nm (DFG-532). By focusing the laser beam onto the metallized AFM tip, we were able to probe the optical properties with...
Fig. 4 Screening length of excitons in heterostructure and the effect of hybridization on the exciton resonance in WSe$_2$ trilayer. a, b Near-field images of the normalized amplitude $s_j(\omega)/s_j(h-BN)$ and phase $\varphi_j(\omega) - \varphi_j(h-BN)$. The images in the left and right panels were taken at 1.68 eV (around the monolayer WSe$_2$ exciton resonance energy) and 1.57 eV (around monolayer MoSe$_2$ exciton resonance energy), respectively. The boundaries of the materials are displayed with dash lines. The scale bars indicate 400 nm. c Line profiles of the normalized amplitude and phase across the monolayer and heterobilayer along the black lines in the right panels in (a and b). d, e Normalized scattering amplitude $s_j(\omega)/s_j(h-BN)$ and phase $\varphi_j(\omega)$ spectra for WSe$_2$ trilayer (data points). The near-field data are fitted by the point dipole model (solid curves). The vertical blue dashed and solid lines in e are used to mark the exciton energies of WSe$_2$ monolayer and WSe$_2$ trilayer extracted from the point dipole model, respectively.

subwavelength resolution. To this end, the back-scattered light is registered by pseudo-heterodyne interferometric detection and then demodulated at the $n$-th harmonics of the tapping frequency yielding background-free images. To eliminate the background, we chose $n = 4$ and 5 in this work. In addition to the background elimination, the high harmonic signal can also reduce the detection depth, which is essential to detect the atomically thin TMDs.

Data availability
Raw files containing the unprocessed near-field images are available from the corresponding author upon reasonable request.

Code availability
Code used to fit the near-field spectra is available from the corresponding author upon reasonable request. This code is based on the NearFieldOptics python package, downloaded from a github repository from Alexander S. Mcleod (https://github.com/asmcleod/NearFieldOptics).

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