Photoneutron spectrometry by novel multi-directional spherical neutron spectrometry system

Mehdi Sohrabi* & Amir Hakimi

Neutron spectrometry in science and technology applications in general and accurate exotic photoneutron (PN) dosimetry of cancer patients undergoing high-dose high-energy X-rays therapy in medical accelerators in particular is of vital need. In this study, a novel passive multi-directional multi-detector neutron spectrometry system was developed and home-made using 6 polycarbonate/10B detectors on 6 sides of polyethylene (PE) cubes used bare and also embedded at center of PE spheres of 8 different diameters. The system provided well-resolved unfolded directional PN spectra showing thermal and fast PN peaks of 6 sides and mean spectrum in 5 field sizes at isocenter and other locations in 18 MV Siemens ONCOR medical linear accelerator bunker. The neutron spectrometry system developed has unique characteristics such as being simple, efficient, low cost, practical, and insensitive to low-LET radiation with well-resolved directional and mean spectra easily applicable in medicine, health, environment, science and technology in developing and developed laboratories.

Neutron spectrometry is of vital need in many areas of health, medicine, environment, science and technology, in particular for accurate exotic photoneutron (PN) dosimetry of cancer patients undergoing high-dose high-energy X-ray therapy in medical linear accelerators for estimating undesired second primary cancer risks of organs1,2. Albeit the complexity, some neutron spectrometry methods have been advanced such as proton recoil method3, time of flight measurements4, threshold detectors5, 3He nested neutron spectrometer2, ultra-thin 3D silicon sensors6 and multi-sphere methods. In particular, Bonner-type polyethylene (PE) spheres coupled with embedded thermal neutron detectors such as activation detectors2,7–9; BF3 or 3He proportional counters2,10–12; CR-39/10B13–16; bubble detectors17–19; paired LiF TLDs20,21; and thermal neutron pulsed detectors22, have been practical and well-adapted methods.

Due to neutron-weighting-factor dependence on neutron energy23 and need to advance scientific developments, determination of directional neutron spectrum due to neutron scattering in the surrounding environmental media is of vital need. In order to better justify this need, two directional dependencies in neutron detection and spectrometry are defined here:

1. Inherent directional dependence of a thermal neutron detector embedded in a PE sphere, and
2. Geometric directional dependence of the neutron spectrometry system which is affected by its geometry and surrounding environmental media at the spectrometry location.

The geometric directional dependence is extremely important in accurate neutron dosimetry of workers in work environments and of patients undergoing high energy X-ray therapy or possibly neutron therapy. Some of the reasons may include:

a. Radiobiological effects of neutrons which depend on neutron energy being itself highly affected by directional dependence of the system and surrounding media,
b. Accurate determination of individual dose equivalents in a work environment requiring accurate directional neutron workplace monitoring, and
c. Accurate determination of patients’ fast, epithermal and thermal PN doses separately and as sum value for estimating the second primary cancer risks of organs1.

Health Physics and Dosimetry Research Laboratory, Department of Energy Engineering and Physics, Amirkabir University of Technology, Tehran, Iran. *email: dr_msohrabi@yahoo.com
To fulfill such needs, some directional neutron spectrometry methods have been advanced such as: super-
heated emulsions at the center of one single 30 cm diameter nylon-6 moderating-sphere with a telescope-design
wherein the detector views a narrow solid angle of about 1/6 steradians from an Am-Be source\textsuperscript{19}, multiple
thermal neutron pulsed detectors in one moderating sphere exposed externally to Am-Be neutrons from dif-
terent directions\textsuperscript{22}, three orthogonal \textsuperscript{3}He tubes used inside a single high-density PE sphere exposed to Am-Be
neutrons\textsuperscript{31}, and design of an ultra-sensitive single cylindrical moderator directional neutron spectrometer based
on seven \textsuperscript{4}He detectors applied to low-fluence cosmic-ray-induced neutrons at ground level\textsuperscript{34}. These advances
are indeed strong supports to vital need to a simple passive multi-directional neutron spectrometry system.

In fact, a neutron spectrometry system should have a detection system with high sensitivity to neutrons, no
sensitivity to low-LET radiation (x, y and β), simplicity in particular in operation, post-exposure time inde-
pendence, easy to be home-made, wide applications when established, and of course capability to determine
directional spectrum. In this context, a passive multi-directional multi-detector spherical neutron spectrometry
system was hypothesized, designed, and developed in this study to fulfil such requirements. The neutron spec-
trometry system developed was then successfully applied to an exotic application; i.e. PN spectrometry in high-
dose high-energy X-rays at the isocenter and some locations in the radiotherapy bunker of a Siemens ONCOR
18 MV X-ray medical linear accelerator (here after called medical accelerator). The detection method is based
on applying the “Sohrabi neutron dosimetry methods” using polycarbonate track detectors (PCTD)/\textsuperscript{10}B thermal
neutron detector when PCTDs are processed by electrochemical etching (ECE) methods\textsuperscript{25–30}. The directional-
sensitive system is based on a PE cube having one PCTD/\textsuperscript{10}B at each of its six sides. The PE cube is used either
as bare, with no PE sphere, or embedded at the center of 8 Bonner-type PE spheres of different diameters. This
design provides a potential to determine neutron spectrum of each of 6 sides of the PE cube and in turn to obtain
a mean neutron spectrum of the point where neutron spectrometry is made.

Having said the above, it is the purpose of this study to;

1. Introduce a novel passive multi-directional multi-detector spherical neutron spectrometry system which
applies 6 PCTD/\textsuperscript{10}B detectors on 6 sides of a PE cube used either as bare or embedded at center of 8 PE
spheres of different diameters,
2. Apply the developed system for directional PN spectrometry in an exotic high-dose rate 18 MV X-rays in a
medical accelerator, and
3. Determine and report directional PN spectra at 5 different field sizes and locations such as at the isocenter, at
50 cm from the isocenter and at the maze-room junction of the radiotherapy bunker, in order to demonstrate
its potential for other normal applications in medicine, health, environment, science and technology.

**Experiments and methods**

**Passive multi-directional multi-detector spherical neutron spectrometry system.** A passive
multi-directional multi-detector spherical neutron spectrometry system was designed, home-made and applied
in PN spectrometry in high-dose high-energy X-ray beam and other locations of a medical accelerator bunker;
which is under extreme and exotic conditions of having a very low PN fluence in the presence of high-dose rate
18 MV X-rays. The spherical neutron spectrometry system consists of three main components including:

1. A base PCTD/\textsuperscript{10}B thermal neutron detector,
2. A central PE cube holding 6 PCTD/\textsuperscript{10}B thermal neutron detectors on its 6 sides, and
3. Eight PE spheres of 2, 3, 4, 5, 6, 8, 10 and 12 inch diameters having a hollow cube carved at their centers in
order to embed the PE cube.

**Base PCTD/\textsuperscript{10}B detector.** The PCTD/\textsuperscript{10}B detector has been recently applied for extremely low-level PN dosi-
metry in 6 MV X-ray beams\textsuperscript{31}, in 18 MV X-ray beams\textsuperscript{4,5,7,8,17,20,32,33} and in a plasma focus device filled with deu-
terium gas\textsuperscript{29}. PCTDs are highly sensitive to 1.47 MeV alpha particles through \textsuperscript{10}B(n\textsubscript{th},α)\textsuperscript{7}Li reaction (high cross
section of 3840 barn), with near 100% efficiency when in contact with enriched \textsuperscript{10}B converter after processed by an ECE method\textsuperscript{25–30}. It should be mentioned that PCTDs basically detect fast neutrons with energy > 1 MeV
through fast-neutron-induced recoil particles by elastic scattering with hydrogen, carbon, and oxygen atoms.
In particular, PCTD/\textsuperscript{10}B detectors when decorated with or without cadmium can be used in neutron dosimetry with minimum detection levels of ~ 1.0 mSv, ~ 0.014 mSv and ~ 0.016 mSv for fast, epithermal and thermal neu-
trons respectively\textsuperscript{34,35}.

After the necessary exposures were made, the PCTDs were removed from the spectrometry system and
processed by the ECE method. Then mean track densities were determined by counting the alpha tracks under
a light microscope. Accordingly, thermal PN fluences were obtained by converting a mean track density ± SD
(tracks.cm\textsuperscript{-2}) of each PCTD/\textsuperscript{10}B detector to fluence by using relevant conversion factors.

**Central polyethylene cube.** In order to compensate for the inherent detector directional dependence and the
geometric system directional dependence of the neutron spectrometry system, six PCTD/\textsuperscript{10}B detectors were
installed on 6 sides of a 4 cm × 4 cm × 4 cm PE cube. One PE cube was used as bare, with no PE sphere, and 8
PE cubes were embedded at the center of 8 PE spheres of different diameters. This design makes the PE sphere
system to multi-directionally respond to neutrons coming from the main beam and from 5 other directions. Fig-
ure 1 shows schematic design of a PE cube with 6 PCTD/\textsuperscript{10}B detectors on sides A, B, C, D, E, and F of the cube.
**Polyethylene moderating spheres.** The basic neutron energy thermalizing medium of this neutron spectrometry system is the PE spheres of different diameters used. The rationale in using PE material (C\(_2\)H\(_4\))\(_n\) is that fast neutrons by interacting through elastic scattering with the atom constituents in particular hydrogen atoms are thermalized and detected by each side thermal neutron detector. As the size of the PE sphere increases, more energetic neutrons are thermalized and detected. Therefore, having PE spheres of different diameters in an increasing order allows detecting fast neutrons with more energy ranges.

In this study, a set of 8 specially-designed PE spheres (\(\rho = 0.9 \text{ g cm}^{-3}\)) with 2, 3, 4, 5, 6, 8, 10 and 12 inch diameters were home-made and used. Each PE sphere consists of two halves with a hexagonal cavity carved at the center to embed the PE cube with 6 PCTD/10B when assembled together. Figure 2a,b shows a PE sphere with a PE cube having 6 PCTD/10B detectors on sides as embedded; (a) in the hexagonal cavity of a half sphere, and (b) at the center of a PE sphere placed at the isocenter of the medical accelerator beam to be exposed. In order to get the full neutron spectrum at each location, each of the 8 spheres has been independently placed one by one at the same location and exposed to equal 18 MV X-ray doses of 5 Gy. In order to block external thermal neutrons from entering the PE sphere, each PE sphere was covered by a cadmium sheet with a thickness of 0.5 mm optimized in a previous study.[31]

**Electrochemical etching of polycarbonate detectors.** Each PCTD used in a PCTD/10B detector is 3.1 cm × 3.1 cm in size and 250 µm thick cut from a larger polycarbonate sheet. Polycarbonate sheets are masked on both sides to prevent any scratches and are commercially available in common plastic markets. The masks are removed when placed on the PE cube to be exposed. The PCTDs after exposure to PNs were processed by a high frequency–high voltage (HF–HV) ECE method under optimized ECE field conditions of 2 kHz–32 kV cm\(^{-1}\) in PEW solution (15 g KOH + 40 g C\(_2\)H\(_5\)OH + 45 g H\(_2\)O) at 26 ± 1 °C for 3 hours.[25–30]

**Medical accelerator bunker.** PN spectrometry studies were performed in the 18 MV X-ray beam and two other locations of a Siemens ONCOR dual energy medical linear accelerator bunker (Siemens Healthcare, Erlangen, Germany). The medical accelerator is equipped with double-focused multi-leaf collimators consisting of 41 leaves of 1 cm resolution at the isocenter. Determination of PN spectra was performed at different locations from which 3 major locations are reported here such as; (1) isocenter (source to center of PE sphere: 100 cm), (2) 50 cm from the isocenter (on patient treatment couch) and (3) maze-room junction. Figure 3 shows schematically the accelerator bunker with measurement locations 1, 2 and 3 in the treatment bunker.

As it was stated above, each of the 8 PE spheres has embedded a PE cube with 6 PCTD/10B detectors on sides. At each measurement location, the bare PCTD/10B and each of 8 PE spheres were exposed at a time to 5 Gy of 18 MV X-ray dose (at a depth of maximum dose) under a 10 × 10 cm\(^2\) X-ray field with respect to standard exposure conditions defined by TRS-398 (IAEA 2000).[36]
Figure 2. (a) Halves of a PE sphere with a PE cube embedded (with 6 PCTD/10B detectors on the sides); and (b) the assembled PE sphere with embedded PE cube as placed at the isocenter of the medical accelerator beam to be exposed.

Figure 3. Three PN spectrometry measurement locations shown inside the radiotherapy treatment bunker of the medical accelerator (darker shaded regions are high density concrete).
Photoneutron spectrum unfolding processes. Unfolding of PN energy spectrum. In situations where neutron energy spectra need to be determined, unfolding the neutron spectrum data is necessary. Neutron spectrometers generally do not directly determine neutron spectra. The basic experimental data usually come folded with the response of the used neutron detector. The energy spectra can be then estimated from the experimental data through a backward process called unfolding.

The relation between detector responses and neutron spectra can be written as Eq. (1):

$$A_i = \int_0^\infty R_i(E) \cdot \varphi(E)dE \quad i = 1, 2, \ldots, n.$$  

(1)

In Eq. (1), $n$ is the number of detectors, $A_i$ is the response of the $i$-th detector, $R_i(E)$ is the $i$-th detector response as a function of neutron energy and $\varphi(E)$ is neutron energy flux. Mathematically, the problem is the case of the Fredholm integral equation of the first kind. It does not have a unique solution, because a finite number of discrete measurements cannot define a continuous function. Therefore, the Eq. (1) can be rewritten in a matrix form as presented in Eq. (2):

$$A = R \cdot \varphi,$$  

(2)

where $A$ is $n \times 1$ vector of dosimeter response, $R$ is $n \times m$ matrix of detector responses and $\varphi$ is $m \times 1$ vector of neutron energy flux. A number of mathematical methods have been applied to solve the problem such as least squares, iterative and Monte Carlo methods. In general, unfolding can be supposed as a mapping, from $n$ dimensional space of detector response to $m$ dimensional space of neutron energy flux.

The most complex aspect of neutron spectrometry with PE spheres is the unfolding process, due to the non-uniqueness of the solution. The unfolding of the PN spectrum determined by PE spheres is associated with several uncertainties from different sources such as those associated with the measurements, detector calibration and response functions\cite{13,37,38}.

To unfold a neutron spectrum data obtained by a spectrometry method, some unfolding methods such as Monte Carlo\cite{37,38}, parameterization and iterative procedures have been used. The time-consuming procedure and low-resolution spectrum of some methods applied\cite{13,37,38}, motivated development of some complementary procedures such as maximum entropy Genetic Algorithms (GA) and Artificial Neural Networks (ANN)\cite{13,39,40}. The ANNs are now being used in a wide variety of data processing applications. The ANN technique is suitable for unfolding the neutron spectra and has some advantages such as saving time and requiring few samples.

Artificial neural network (ANN) PN unfolding method. The unfolding process of the neutron energy spectrum using the ANN method is described. ANNs are mathematical models that are designed to think like the human brain\cite{41,42}. Neural network models include interconnected groups of artificial neurons that imitate the function of neuron cells. Neural network models can learn from data using determined training rules\cite{41,43}. Actually, neurons are the basic processing units of a network. A neuron takes weighted summation of multiple inputs to produce an output in accordance with a user specified transfer function. The weights for the inputs are known as "synaptic-weights". A network can be regarded as a function that maps inputs to outputs. During the training process, a network adapts the synaptic-weights for a desired purpose\cite{41,43}.

In the present study, to unfold the raw data obtained, an ANN-based code Multisphere Neutron Spectrometry Unfolding Code (MNSU+) for each MU was developed by us and used by which each set of PN fluence data at the center of each PE sphere was deconvolved into a 25-bin neutron energy spectrum. Practically, unlike other known and commonly used neutron unfolding methods, there is no need to form response matrix in ANN unfolding methods. Actually, in the other unfolding methods, the detection and evaluation were carried out in two steps; performing the measurement and unfolding of the detector responses. All of the unfolding methods need the detector response matrix for solving the problem and some of them need prior information about spectra. However, the neural networks are trained once, and then the trained neural network is used for unfolding, which takes a very short time without the need for a detector response matrix and any prior information\cite{44,47}.

In the MNSU+, a simple linear ANN architecture without biases and hidden layers has been developed and trained for unfolding PN spectra. In each state, the PN fluence data at the center of each PE sphere and the generated PN energy spectrum are considered as input and output data of the ANN, respectively. In the training mode, the network is presented with a set of inputs corresponding to known outputs. During the training it learns the rules that produce the outputs from the inputs and the weights are adjusted to present the closest outputs to the real outputs. In this study, the training data are sets of neuron spectra defined from thermal to 630 MeV in sixty energy groups and the corresponding responses of Bonner spheres taken from IAEAs Compendium of neutron spectra and detector responses for radiation protection purposes (IAEA Technical Report Series No.318)\cite{38}, a set of response functions of monoenergetic neutrons at the center of each PE sphere provided by Standard Dosimetry Laboratory of the National Radiation Protection Department (Tehran, Iran) and determined at the center of each PE sphere and also calculated by simulation using MCNP 4C Monte Carlo code. The training method is the resilient backpropagation algorithm. An energy spectra measurement system was also set up for the validation of the unfolding capability by using a $^{252}$Cl neutron source. The resultant unfolded $^{252}$Cl source spectrum is in agreement with the results provided in the literature for neutron spectrometry\cite{11,20,22,37,38,49}.

Experimental findings and results

Photoneutron spectrometry of 3 major locations in the radiotherapy bunker of the medical accelerator was carried out in particular at the isocenter with different field sizes using the multi-directional neutron spectrometry system developed in this study. One bare PE cube with 6 side PCTD/10B detectors and 8 PE spheres embedding
PE cubes at their centers have been exposed one at a time at each location under the same 18 MV X-ray dose of 5 Gy. Each measurement location simply leads to 54 data points based on which the PN fluences have been determined for all the 6 directions. Each side detector of a PE cube, used either as bare or as embedded in a sphere, at each measurement location provides spectrum data different from those of other sides of the PE cube. This is due to scattering of fast PNs from the surrounding media caused by different geometry conditions in locations in the radiotherapy bunker. Such variations can be well demonstrated by plotting the 54 data points taken at each of the 3 measurement locations in the radiotherapy bunker as functions of the PE sphere diameter. Figure 4a–c demonstrates the PN fluence versus PE sphere diameter for each PCTD/10B detector on each side of the PE cube at 3 spectrometry locations in the bunker at: (a) isocenter, (b) 50 cm from the isocenter, and (c) maze-room junction for 5 Gy dose of 18 MV X-rays in a 10 × 10 cm² field of the medical accelerator.

By direct analysis of the 3 sets of responses of Fig. 4a–c, some conclusions follow:

1. In order to better analyze the PN fluence versus PE sphere diameter responses, one has to understand what each PCTD/10B on a PE cube side detects. In general, each side PCTD/10B detects neutrons from all directions, but preferably from the side facing the side. For example, the PCTD/10B on side A at the isocenter primarily detects neutrons coming from the direct beam and those coming from scattered PNs of other directions. Therefore, since thermal neutron fluence directly from the beam is relatively low, the full thermal neutron response of the side A is below those of the sides B and D which receive more thermalized neutrons from the surrounding media. Such explanations can be extended to also other side detector responses.

2. The data of the bare PE cube with detectors on sides have the lowest values in all 3 sets of responses. In particular, at the isocenter, they have more or less the same values close to each other. These values are more diverted at other two PN spectrometry locations.

3. In all 3 sets of responses, 5 cm diameter sphere data show maximum thermal neutron fluences or peaks for each of 6 sides.

4. The responses of the 30 cm diameter PE sphere at the maze-room junction is about 10 times lower than relevant data at the isocenter and at 50 cm from the isocenter due to the PN spectrum being well softened at that spectrometry location.

5. The responses at the isocenter are more structured relative to each other with the same trend while those of the other two spectrometry locations are more diverted.

The PN spectra at the three stated locations were all determined with X-ray dose of 5 Gy. However, such data are reported in Table 1 as PN fluence per MU for six PCTD/10B detectors on sides A, B, C, D, E, and F of PE cubes embedded at the centers of all 8 PE spheres exposed at the isocenter based on which the PN spectra and their mean spectrum have been determined.

Applying the basic data given in Table 1, the PN spectra determined by 6 PCTD/10B detectors on 6 sides of the 9 PE cubes (one bare and 8 embedded in PE spheres) as exposed at the isocenter to 5 Gy 18 MV X-ray dose in a 10 × 10 cm² field are shown in Fig. 5 (a, b, c, d, e, f).

By direct analysis of the basic data the PN spectra given in Table 1 and in Fig. 5a–f, some conclusions can be drawn;

1. Regardless of the side of the PE cube, the general shape of the PN spectra of the 6 side detectors are close to each other and well demonstrates two peaks; one thermal PN peak with an epithermal and intermediate energy tail followed by another peak for fast PNs within 0.05 to 1.0 MeV²,8,31,39,40,50,51.

2. Thermal PNs have small contribution, while fast PNs have the largest influence on the total PN dose equivalent. Previous studies showed that about 90% of PN dose equivalent was contributed by fast PNs with energy above 0.5 MeV²,7,6,13,20,32,35,40,51.

3. The PN fluences determined by detectors on 6 sides of the PE cube are quite different. For example, the PN fluences on the sides C and F are in general lower than the others almost at all energies.

It has been recently demonstrated by us that fast, epithermal and thermal PN dose equivalents increase linearly as field size increases for field sizes 10 × 10, 20 × 20, 30 × 30 and 40 × 40 cm² studied, as also discussed by others²,3,15,25,52,53. This can be due to less attenuation of the PNs by the accelerator head material components as the field size increases, and less scattering from the target, beam flattening filter and primary collimator. This effect of course can cause the neutron spectrum to differ from one field size to another. Therefore, in order to further verify this concept by PN spectrometry, the PN spectra of 5 field sizes 0 × 0, 10 × 10, 20 × 20, 30 × 30 and 40 × 40 cm² were determined at the isocenter. Figure 6a,b shows PN spectra of 5 field sizes; (a) 0 × 0, 10 × 10 and 20 × 20 cm², and (b) 30 × 30 and 40 × 40 cm² as exposed at the isocenter to 5 Gy 18 MV X-ray dose.

The PN spectra in Fig. 6a, b for the 5 field sizes well demonstrate an increase in the PN fluence and are hardened in neutron energy as the field size has increased. However, in order to better demonstrate the effects of field size on the PN fluence, the PN fluence as functions of diameter of the PE spheres for 5 different field sizes 0 × 0, 10 × 10, 20 × 20, 30 × 30 and 40 × 40 cm² are shown in Fig. 7.

The PN fluence versus PE sphere diameter responses of Fig. 7 well demonstrate that as the field size has increased, the PN fluence at all energies has increased. This observation indicates also that the mean energy of PNs in general has increased as the field size has increased, as shown in Fig. 8. The PN mean energy versus field size response as shown in Fig. 8 is linear and the mean PN energies obtained are 0.44 ± 0.01, 0.48 ± 0.02, 0.50 ± 0.03, 0.51 ± 0.04, 0.53 ± 0.03 MeV respectively for field sizes 0 × 0, 10 × 10, 20 × 20, 30 × 30 and 40 × 40 cm².

By direct analysis of the 5 PN energy spectra of 5 field sizes, as shown in Figs. 6a,b, 7 and 8, some conclusions follow;
1. All five PN energy spectra of 5 field sizes of Fig. 6a,b demonstrate a common spectrum trend with two peaks; one thermal PN peak followed by a tail of epithermal and intermediate energy PNs before reaching a fast PN peak, as has also been observed by others.2,13

2. As field size has increased, the PN fluence levels at all energies have increased. In particular, the heights of the thermal and fast PN peaks have increased as the field size has increased; i.e. the peak heights are the lowest for the 0 × 10 cm² field and the highest for 40 × 40 cm² field sizes.

3. The mean PN energy has also increased as the field size has increased (Fig. 8).

Figure 4. Photoneutron fluence versus diameter of the PE spheres for all six side PCTD/10B detectors as determined at 3 spectrometry locations in the radiotherapy bunker; (a) isocenter, (b) 50 cm from isocenter, and (c) maze-room junction for 5 Gy dose of 18 MV X-rays in a 10 × 10 cm² field of the medical accelerator.
The above conclusions are all in support of the findings that the fast, epithermal and thermal PN dose equivalents increase linearly as field size increases\textsuperscript{13,31,33,50,52,53}.

As shown in Fig. 6a,b, the PN spectra obtained at the isocenter have a low-height thermal fluence peak and a sharp large peak due to fast neutrons. While the fast neutron peak can be more or less related to the main beam, the thermal PN peak is partly from the beam and partly from fast PNs thermalized and reduced in energy through elastic scattering with atomic constituents of the material in the accelerator head, and surrounding media. Such elastic scattering interactions in fact make the PN spectra in a high energy X-ray therapy bunker vary from location to location. Therefore, in order to further demonstrate such variations, PN spectra of different locations in the radiotherapy bunker at the three locations namely the isocenter, 50 cm from the isocenter and at the maze-room junction are compared, as shown in Fig. 9. The X-ray dose was 5 Gy in a 10 × 10 cm\textsuperscript{2} field size of the 18 MV X-ray beam.

By analyzing the 3 PN spectra of Fig. 9 at the 3 stated locations comparatively, some conclusions follow:

1. The PN spectrum has been strongly softened when distance from the isocenter to the other two locations has increased; slightly at 50 cm from the isocenter and strongly at the maze-room junction.
2. The thermal PN peak height of each PN spectrum strongly increases and the fast PN peak height strongly decreases as distance has increased from the isocenter to the maze-room junction. This is due to softening of the fast PNs scattered by the surrounding media.
3. The neutron spectrometry system developed was demonstrated being highly sensitive to detect any small changes occurred in the PN fluence and energy at different spectrometry locations in the radiotherapy bunker. In fact, the PN spectra at different locations of the maze which have very low PN fluences with relatively softer spectra have been determined which demonstrate the stated claim and will be reported elsewhere.

The general shape of the PN spectra are in good agreement with those of other studies using different PE sphere spectrometry methods with other central thermal PN detectors such as activation foils\textsuperscript{31,40}, superheated

### Table 1.

| Energy (MeV) | Photoneutron Fluence per MU (n cm\textsuperscript{-2} MU\textsuperscript{-1}) |
|-------------|---------------------------------|
| A           | B                               | C       | D       | E       | F       | Mean   |
| 1.03E−09    | 1.02E+04                        | 1.03E+04| 9.05E+03| 1.10E+04| 8.36E+03| 1.01E+04| 9.84E+03|
| 5.78E−09    | 6.57E+04                        | 6.57E+04| 2.70E+04| 7.19E+04| 5.13E+04| 6.50E+04| 6.29E+04|
| 1.87E−08    | 3.14E+05                        | 3.14E+05| 2.75E+05| 3.45E+05| 2.49E+05| 3.12E+05| 3.02E+05|
| 3.28E−08    | 6.96E+05                        | 6.96E+05| 6.04E+05| 7.02E+05| 5.44E+05| 6.89E+05| 6.66E+05|
| 5.78E−08    | 6.93E+05                        | 6.93E+05| 6.46E+05| 7.62E+05| 5.51E+05| 6.88E+05| 6.66E+05|
| 1.03E−07    | 3.41E+05                        | 3.41E+05| 2.98E+05| 3.75E+05| 2.71E+05| 3.38E+05| 3.28E+05|
| 3.28E−07    | 2.97E+05                        | 2.97E+05| 2.90E+05| 3.26E+05| 2.36E+05| 2.95E+05| 2.86E+05|
| 1.03E−06    | 1.90E+05                        | 1.90E+05| 1.64E+05| 1.88E+05| 1.49E+05| 1.87E+05| 1.82E+05|
| 3.28E−06    | 1.70E+05                        | 1.70E+05| 1.47E+05| 1.86E+05| 1.31E+05| 1.67E+05| 1.62E+05|
| 1.03E−05    | 1.67E+05                        | 1.67E+05| 1.44E+05| 1.81E+05| 1.31E+05| 1.64E+05| 1.60E+05|
| 3.28E−05    | 1.69E+05                        | 1.69E+05| 1.47E+05| 1.86E+05| 1.34E+05| 1.67E+05| 1.62E+05|
| 1.03E−04    | 1.65E+05                        | 1.65E+05| 1.44E+05| 1.81E+05| 1.31E+05| 1.63E+05| 1.58E+05|
| 3.28E−04    | 1.66E+05                        | 1.66E+05| 1.44E+05| 1.82E+05| 1.32E+05| 1.64E+05| 1.59E+05|
| 1.03E−03    | 1.61E+05                        | 1.61E+05| 1.40E+05| 1.85E+05| 1.30E+05| 1.58E+05| 1.55E+05|
| 3.28E−03    | 1.97E+05                        | 1.97E+05| 1.51E+05| 2.54E+05| 1.31E+05| 1.93E+05| 1.89E+05|
| 1.03E−02    | 2.06E+05                        | 2.06E+05| 1.79E+05| 2.64E+05| 1.66E+05| 2.02E+05| 1.97E+05|
| 3.28E−02    | 4.00E+05                        | 4.00E+05| 3.52E+05| 4.33E+05| 3.24E+05| 3.93E+05| 3.84E+05|
| 5.78E−02    | 9.79E+05                        | 9.79E+05| 7.62E+05| 1.07E+06| 7.93E+05| 9.62E+05| 9.42E+05|
| 1.03E−01    | 1.66E+06                        | 1.66E+06| 1.36E+06| 1.81E+06| 1.65E+06| 1.63E+06| 1.60E+06|
| 1.87E−01    | 2.27E+06                        | 2.27E+06| 2.02E+06| 2.41E+06| 1.89E+06| 2.27E+06| 2.19E+06|
| 3.28E−01    | 1.36E+06                        | 1.36E+06| 1.21E+06| 1.47E+06| 1.29E+06| 1.36E+06| 1.31E+06|
| 5.78E−01    | 1.09E+06                        | 1.09E+06| 9.74E+05| 1.18E+06| 8.77E+05| 1.09E+06| 1.05E+06|
| 1.03E+00    | 5.52E+05                        | 5.52E+05| 4.89E+05| 5.97E+05| 4.35E+05| 5.45E+05| 5.29E+05|
| 1.87E+00    | 5.49E+04                        | 5.49E+04| 4.95E+04| 5.09E+04| 4.73E+04| 5.43E+04| 5.27E+04|
| 1.03E+01    | 2.89E+03                        | 2.89E+03| 2.56E+03| 3.12E+03| 2.28E+03| 2.85E+03| 2.77E+03|
drop detectors\textsuperscript{50}, thermoluminescence detectors\textsuperscript{13,39,40} and CR-39\textsuperscript{51}, as well as simulation of the medical accelerator head and treatment conditions by using simulation codes\textsuperscript{2,49,50}.

Figure 5. (a–f) PN spectra determined by the 6 PCTD/\textsuperscript{10}B detectors fixed on 6 sides A, B, C, D, E, and F of PE cubes (one bare and 8 embedded in 8 PE spheres) exposed to PNs at the isocenter to 5 Gy 18 MV X-ray dose in the 10 × 10 cm\textsuperscript{2} field.
Figure 5. (continued)
Discussions

The rationale for developing the passive multi-directional multi-detector spherical neutron spectrometry system in this study is its high sensitivity to neutrons, insensitivity to low-LET radiation (x, y and β) and non-ionizing radiation, negligible inherent geometric directional dependence, no post-exposure fading, simple and small detectors, easily home-made, no need to sophisticated detectors/instruments, reproducible in any developing or developed laboratories, low cost, no need to cable connection, scalable and applicable to other applications from small to mega-size detectors, simple record keeping of processed detectors, ease of manpower training, and in particular capable in determining directional and mean neutron spectra of a mixed neutron-gamma field. The neutron spectrometry system developed fulfils these requirements in particular the PE spheres are isotropic in response and have negligible inherent geometric directional dependency compared to other PE moderator...
geometries. The insensitivity of PCTDs to low-LET radiation has been proved in our pioneering studies by exposing them to a γ dose of $10^2$ Gy from a $^{137}\text{Cs}$ source\textsuperscript{32}.

Albeit the unique characteristics of the passive neutron spectrometry system developed, it has some disadvantages such as lack of online provision of data (like any other passive systems), need to ECE processing for PCTDs by applying high voltage power supplies at a certain frequency (what some laboratories might have hesitations to apply; but if CR-39 is used, chemical etching can be used), and also manual track counting when an automatic track counting system is not applied. In fact, if the system is well established by a developing or developed laboratory or a service provider, services may be provided for national, regional, and possibly international scientific collaborations or for provision of commercial services to other laboratories at a reasonable cost. This approach can be simply made by only mailing PE cube (s) with 6 PCTD/$^{10}$B thermal neutron detectors on

Figure 6. PN spectra of 5 field sizes; (a) $0 \times 0$, $10 \times 10$ and $20 \times 20$ cm$^2$ and (b) $30 \times 30$ and $40 \times 40$ cm$^2$, by the PE sphere neutron spectrometry system developed as exposed at the isocenter to 5 Gy 18 MV X-ray dose.
Figure 7. Photoneutron fluence versus PE sphere diameter for $0 \times 0$, $10 \times 10$, $20 \times 20$, $30 \times 30$ and $40 \times 40$ cm$^2$ field sizes at the isocenter exposed to 5 Gy 18 MV X-ray dose.

Figure 8. Photoneutron mean energy versus field side for field sizes $0 \times 0$, $10 \times 10$, $20 \times 20$, $30 \times 30$ and $40 \times 40$ cm$^2$ at the isocenter of 18 MV X-ray beams of the medical accelerator.
sides; being passive system in fact is highly advantageous. Only one or two cubes with some additional PCTDs are enough since only one PE sphere is exposed at a time and only the PCTDs can be changed and the same cube can be reused. The service providing laboratory or company then receives the exposed PCTDs, processes them, count the tracks either manually or by a processing system, unfolds the data and reports the results; either as scientific collaborations or by payment. The laboratory receiving services can only prepare a set of PE spheres in order to obtain the full neutron spectrum, or by any other arrangements needed31. Another added value of this passive system is insensitivity to low-LET radiation so that it can be used in exotic or extreme mixed field radiation applications such as on board of space shuttle and international space stations as well as for other cosmic ray studies, if online information can be tolerated. In particular, the system as being passive can be exposed to

**Figure 9.** The PN spectra determined at 3 locations in the accelerator bunker; the isocenter, 50 cm from the isocenter, and at the maze-room junction in a 10 × 10 cm² field for 5 Gy 18 MV X-rays dose.
cosmic neutrons in an environment for a long time on the ground or at a desired elevation. By this approach, the cosmic neutron spectrum can be determined with very high accuracy.

The multi-directional neutron spectrometry system introduced in this study provides the capability for capturing PNPS directionally as demonstrated in an exotic or extreme application having low fluence neutrons in the presence of 5 Gv of 18 MV X-rays in a medical accelerator. The PNPS spectrometry data reported above demonstrated well-resolved neutron spectra even at situations where the neutron spectra were very close to each other. The PNPS spectra all showed well-resolved thermal PN peaks along with epithermal and intermediate energy tail reaching a fast PN peak the heights of which depend on many factors discussed. The general mean PNPS spectra trend is in good agreement with those of other studies using different PNPS spectrometry methods and of course with differences as regards to X-ray energy, type of head material, type of detector, radiotherapy bunker design and construction material, spectrometry location, etc.

Conclusions
A passive multi-directional multi-detector spherical neutron spectrometry system, with some unique characteristics, as discussed above, was designed, home-made and applied to an exotic PNPS spectrometry in a medical accelerator bunker. The system used 6 PCTD/10B detectors on 6 sides of a PE cube used as bare or embedded at the center of 8 PE spheres of different sizes in order to determine directional neutron spectra and mean spectra of locations of concern in a Siemens ONCOR medical linear accelerator bunker. The neutron spectrometry system was successful in obtaining:

a. Well-resolved PNPS fluence responses as functions of PE sphere diameters for 6 different directions at the isocenter, at 50 cm from the isocenter and at the maze-room junction of the accelerator bunker (Fig. 4a–c),

b. Six well-resolved directional and mean PNPS spectra of a 10 × 10 cm² 18 MV X-ray field at the isocenter as well as mean PNPS spectra of other field sizes and locations (Fig. 5a–f),

c. Five well-resolved mean spectra at the isocenter for 5 field sizes 0 × 0, 10 × 10, 20 × 20, 30 × 30 and 40 × 40 cm² distinctly distinguished from each other (Fig. 6), and

The neutron spectrometry system introduced and used in such an exotic PNPS spectrometry application has well demonstrated that the system can be easily and successfully applied for neutron spectrometry in other areas in medicine, health, environment, science and technology in any developed or developing laboratories.

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Author contributions
M.S. originated the idea, designed and developed the neutron spectrometry system, planned and supervised the experiments by using his neutron dosimetry methods invented and advanced over decades, analyzed and interpreted the results and wrote the submitted paper; A.H. executed the exposures, obtained the data, unfolded the photoneutron spectra and made the graphs as well as contributed to basic draft and literature research in cooperation and under direct supervision of M.S.

Competing interests
The authors declare no competing interests.
