Efficient electroweak baryogenesis by black holes

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Abstract

A novel cosmological scenario, capable to generate the observed baryon number at the electroweak scale for very small CP violating angles, is presented. The proposed mechanism can be applied in conventional FRW cosmology, but becomes extremely efficient due to accretion in the context of early cosmic expansion with high energy modifications. Assuming that our universe is a Randall-Sundrum brane, baryon asymmetry can easily be produced by Hawking radiation of very small primordial black holes. The Hawking radiation reheats a spherical region around every black hole to a high temperature and the electroweak symmetry is restored there. A domain wall is formed separating the region with the symmetric vacuum from the asymmetric region where electroweak baryogenesis takes place. First order phase transition is not needed. The black holes’s lifetime is prolonged due to accretion, resulting to strong efficiency of the baryon producing mechanism. The allowed by the mechanism black hole mass range includes masses that are energetically favoured to be produced from interactions around the higher dimensional Planck scale.
1 Introduction

Baryogenesis is a key question of cosmology. Various interesting models of baryogenesis have been proposed during the last thirty years (see reviews [1]-[6]). An important piece of knowledge extracted from all this research is the realization that it has proved quite difficult to construct a simple model capable to generate the observed amount of baryon asymmetry.

The standard mechanism of baryogenesis demands the concurrent satisfaction of three physical requirements, as it was first explained by Sakharov [7]:

1. Baryon non-conserving processes. This can be achieved either at the grand unification scale [8], or even at the electroweak energy scale [9].
2. C and CP-violation which has already been observed in experiment.
3. Out of equilibrium conditions. This can be realized in an expanding universe in interactions evolving very massive particles, or in a first order phase transition, or due to thermal domain walls around black holes as proposed in the present work.

Baryogenesis by heavy particle decays was first proposed in [7], [10] (see also [11], [12]). Due to heavy particle decays in an expanding cosmology in the presence of C and CP violation, baryon asymmetry is produced. Usually this mechanism can be realized in grand unification models with the heavy particle being a gauge boson of grand unification. Electroweak baryogenesis is another scenario attracted a lot of study [13]. It is natural to expect to generate baryon asymmetry at this energy scale, otherwise rapid sphaleron processes at 100 GeV will destroy any baryon asymmetry produced earlier. The standard model incorporates non-conservation of baryons (through the chiral anomaly) [9], as well as deviation from thermal equilibrium if the phase transition is first order. Unfortunately, the recently discovered heavy Higgs boson turns the transition to a second order one. Another disadvantage of the standard model is its very small CP violating phases [14]. The present work refers to the electroweak energy scale, but solves both problems as it will be shortly explained. There are of course other possibilities too to have baryogenesis at the electroweak scale, like TeV scale gravity [15], [16].

Another way to produce baryon asymmetry is baryo-through-lepto-genesis [17]. At high energies, large as $10^{10}$ GeV, lepton asymmetry is produced from heavy Majorana fermion decays, and subsequently, this lepton asymmetry leads to baryon asymmetry by the equilibrium electroweak processes which break $(B + L)$ symmetry [18]. A different mechanism is the Affleck-Dine baryogenesis [19]. In supersymmetric models scalar superpartners of baryons or leptons can acquire a large baryonic charge after inflation.
Subsequent $B$-conserving decay of these fields transform baryon asymmetry into that in the quark sector. This mechanism, contrary to all others, leads to quite high value of baryon-to-photon ratio of order one, and special effort is needed to generate the observed amount. The proposed mechanism in the current work is also able to generate large baryon asymmetries which, however, can be controlled to have the correct value. Large amounts of baryon asymmetry can also be generated in the so called Spontaneous baryogenesis \[20\], in which a spontaneously broken global $U(1)$ symmetry associated with baryonic number is assumed to exist. Unfortunately, these models are associated to large isocurvature density perturbations at large scales which are forbidden by cosmic microwave background.

Another interesting class of models concerns baryogenesis through evaporation of primordial black holes (PBHs) \[21\]. The particle propagation of the Hawking radiation \[22\] in the gravitational field of the BH distorts the thermal equilibrium and makes possible the creation of a net excess of particles over antiparticles, assuming baryon non conserving heavy particle decays. The scenario presented here assumes the existence of primordial black holes emitting thermal radiation. However, the mechanism for the generation of baryon asymmetry is totally different. There are finally some more exotic scenarios, for example mechanisms based on space separation of $B$ and $\bar{B}$ (these scenarios allow for baryonic charge conservation and globally baryo-symmetric universe) \[23\]-\[25\]. Successful baryogenesis could be realized even without the three Sakharov conditions \[11\], although these mechanisms are somewhat more technically complicated.

Primordial black holes can be very small black holes created at the first moments of the universe \[26\]. The first PBHs baryogenesis models were based on grand unified theories (GUT) \[27\]. GUT processes can truly produce baryon number, but this is subject to sphaleron wash out \[28\]. The electroweak baryogenesis scenario proposed by Cohen, Kaplan and Nelson (CKN model) \[29\] addresses this problem applying the sphaleron process to produce baryon number. Nagatani \[30\], in order to overcome the well known problems of electroweak baryogenesis, proposed a scenario where baryogenesis takes place in a thermal domain wall surrounding small primordial black holes with temperature higher than the electroweak critical temperature $T_W \simeq 100$ GeV. Although the idea in \[30\] is attractive it did not received much interest. One disadvantage is the assumption that the universe should pass from a black hole dominated era after inflation. This is not very natural, although not forbidden, in the context of 4-dimensional cosmology \[51\]. However, it becomes very possible in a universe with early high energy modifications, as e.g. in a brane world cosmology where the creation of PBHs is much more easier due
to the low 5-dim Planck scale. Another disadvantage is the final outcome that only for very large CP violating phases of order one it is possible to produce the required baryon asymmetry and this is true for black holes masses around 100Kgs.

In the present work, first we correct a wrong constraint that was used in [30] and we find that the allowed parameter space for baryogenesis is improved. Second, the present paper studies this baryogenesis mechanism in the context of Randall-Sundrum (RS) brane cosmology [31] and explains how it is possible to get very easily efficient generation of baryon asymmetry even for very small CP violating angles. The allowed by the mechanism BH mass range includes the black hole masses around the higher dimensional Planck mass. The latter is important since this mass spectrum is energetically favorable to be generated from high energy interactions in the very early braneworld cosmic history. Furthermore, the black hole domination era can now be naturally realized due to the accretion in the high energy regime.

Let us explain in more detail the proposed scenario. The existence of extra dimensions [32] is considered possible and a lot of research has been carried out towards higher dimensional cosmological models. Not only the cosmic geometry, but also the properties of black holes in theories with large or infinite extra dimensions are different, since now the fundamental Planck mass is much lower. The proposed scenario of electroweak baryogenesis concerns the baryon asymmetry generation at the domain wall around annihilating PBHs in a universe with extra dimensions and in particular RS-II cosmology [31]. There are various mechanisms for generating these PBHs. After their formation a part of the universe consists of PBHs and the rest consists of radiation at temperatures lower than the electroweak scale. Soon after their formation PBHs start to accrete and evaporate. Depending on the accretion efficiency the two phenomena can dominate each other. The black hole Hawking radiation emitted thermalises the surrounding region at temperatures above the electroweak scale. This results to the creation of a domain wall that connects the two different vacua. As the Hawking particles pass this domain wall experience a CP violation leaving a net baryon asymmetry in the outgoing emitted radiation. At the end of PBHs’ complete evaporation the Universe has been reheated from this Hawking flux at temperatures above the nucleosynthesis scale. The produced baryogenesis is greatly enhanced due to the extended lifetime of the PBHs. The prolonged lifetime is caused by the accretion factor which holds at the high energy cosmic period. In addition, the significant black hole accretion that takes place allows a black hole dominated cosmic era which helps the mechanism.

Electroweak baryogenesis takes place at the domain wall via the standard sphaleron
process [29]. Note that the existence of the symmetric region surrounding the black hole washes out any baryon number created in a prior epoch. The proposed scenario satisfies the Sakharov’s three criteria for baryogenesis [33], [30]. First, the sphaleron process that takes place at the domain wall is a baryon number violating mechanism. Second, although the Standard Model is a chiral theory which incorporates C-asymmetry, this is not large enough. Thus, we assume a two-Higgs doublets extension of the Standard Model [34], [35] as the background field theory because it provides large CP violating phases on the Higgs sector. Finally, the outgoing radiation of the black hole is a non-equilibrium process. A main advantage of this scenario, compared to the CKN electroweak baryogenesis, is the type of the phase transition needed. At the CKN model a first order transition is required. In the present work the domain wall is created by the thermal radiation of the black hole, and so, the phase transition can be of second order [30]. The most important result of this study is the achievement of the observed value of $b/s \simeq 6 \times 10^{-10}$ for very small CP violating angles.

2 Baryogenesis in the standard 4-dim FRW universe

As mentioned in Introduction, the possibility of electroweak baryogenesis by small primordial black holes in the standard 4-dimensional FRW universe was shown in [30]. In order to calculate the baryon-to-entropy ratio $b/s$, the author used for the density of the black holes the Einstein equation for flat universe with matter dominant

$$\rho_{BH} = \frac{1}{6\pi} \frac{m_{pl}^2}{t^2}. \quad (1)$$

Although, the black hole dominated era can be described by $\rho_{BH} \propto a^{-3}$, it is not correct to fix the unknown integration constant, and so this equation is correct up to an unknown prefactor. Indeed, we can not normalise to the present cosmic density since black holes completely evaporate. In addition, it is not possible to determine the prefactor using an initial black hole density at some initial time since both these quantities are unknown and model dependent. In the discussed scenario the initial cosmic density $\rho_{BH}$ at formation is a free parameter since it depends on the details of the black holes generation (inflation or other mechanism). The correction of the mistake means that there is one less constraint for the black hole mass and the scenario becomes more attractive.

Let us now correctly estimate the amount of the produced baryon-to-entropy ratio. The total baryon number created in the lifetime of a black hole is

$$B = \frac{15}{4\pi^2 g_s} N_\kappa \alpha_W^5 \epsilon \Delta \varphi_{CP} \frac{m_{pl}^2}{T_{BH} T_W}, \quad (2)$$
where $g_\ast \simeq 100$ is the number of degrees of freedom that a BH can decay into at the electroweak temperature, $N \simeq O(1)$ is a model dependent constant which is determined by the type of spontaneous electroweak baryogenesis scenario and the fermion content, $\kappa \simeq O(30)$ is a numerical constant expressing the strength of the sphaleron process \cite{36}, $\alpha_W = 1/30$ \cite{37}, $\epsilon \simeq 1/100$, $T_W = 100$ GeV is the electroweak scale, and $\Delta\varphi_{CP}$ is the CP violating angle. The total baryon number density created from all black holes is given by $b = B n_{BH}$, where $n_{BH} = \frac{\rho_{BH}}{m_{BH}}$ is the number density of the black holes assuming a monochromatic spectrum of black holes. The universe after the creation of PBHs is black hole dominated with density $\rho_{BH}$. Soon after black holes almost instantaneous evaporation, the universe is reheated, its density has the form of radiation and is equal to $\rho_{rad}(t_{reh})$. Thus, \begin{equation}
abla \rho_{BH}(t_{reh}) \simeq \rho_{rad}(t_{reh}) = \frac{\pi^2}{30}g_{reh}T_{reh}^4. \tag{3}
abla \end{equation}

The fact that $\rho_{BH}$ is a free parameter allows a freedom on the choice of $T_{reh}$. However, $T_{reh}$ has to be below $T_W$ in order the baryogenesis scenario under discussion to be viable. Note that even if the scenario was working giving finally a baryon asymmetry at reheating temperature larger than $T_W$, this asymmetry would be washed out later when the universe will experience the electroweak transition. In addition, $T_{reh}$ has to be also larger than the nucleosynthesis temperature. Finally, estimating the cosmic entropy density as $s = \frac{2\pi^2}{45}g_{reh}T_{reh}^3$ \cite{38}, we can calculate the total baryon-to-entropy ratio asymmetry.

Choosing $T_{reh} = 90$ GeV it is possible to calculate the total baryon-to-entropy ratio from all black holes

\begin{equation}
\frac{b}{s} = 2.4 \times 10^{-10} \Delta\varphi_{CP}. \tag{4}
\end{equation}

It is obvious that the required for nucleosynthesis amount of baryon asymmetry is achieved only for $\Delta\varphi_{CP} = \pi$. Therefore, the mechanism can hardly provide sufficient baryon asymmetry. For smaller values of $T_{reh}$ the baryon asymmetry is further reduced. Eq. (4) surprisingly does not depend on the black hole mass. Although the black hole mass does not determine the baryon asymmetry, it is constrained from two requirements regarding the existence of thermal stationary domain wall and the black hole lifetime in comparison with the domain wall time scale. These two constraints remain the same as in \cite{30} and give the following range for the initial BH mass

\begin{equation}4.3 \times 10^{28} \text{ GeV} < m_{BH} < 1.1 \times 10^{32} \text{ GeV}. \tag{5}\end{equation}
3  Baryogenesis in the braneworld and black hole mass constraints

In the framework of a RS-II braneworld embedded in a AdS bulk, primordial black holes are produced after the end of inflation or at the very beginning of a non-inflationary flat model. Our scenario does not depend on the details regarding the origin of the PBHs, thus this work does not study this issue. It is well known that the properties of the brane black holes are modified compared to those in a standard cosmology \cite{39, 40}. They are colder and live longer. More important, the accretion of material from the neighborhood of the black hole can be stronger than evaporation during a high-energy regime. This can not occur in the four-dimensional case. The presence of strong accretion has two advantages. First, it can lead to black hole dominated universe, and second, it leads to an extension of the black holes lifetime.

Brane black holes involved in the proposed mechanism are small enough to ensure that Hawking temperature $T_{BH}$ is much greater than the electroweak critical temperature $T_{W}$, and so, all kinds of Standard Model (SM) particles emitted on the brane are in the symmetric phase. There is also emission towards the bulk, although much less, where only gravitons are assumed to radiate. Being interested in baryogenesis, we have to deal with the emission on the brane. The emission on the brane causes the thermalization of the surrounding region which contains radiation at low temperature. Local thermalization applies to a region where particles have a mean free path (MFP) smaller than the size of this region. Thus, a local temperature $T(r)$ can be defined and the mean free path of a particle $f$ is given by $\lambda_f(T) = \frac{\beta_f}{T}$, where $\beta_f$ is a constant depending on the particle species only. The quarks and the gluons have a strong interaction and they have the shortest MFP with $\beta_s \simeq 10$.

For a black hole with temperature $T_{BH}$ there is always a closely neighborhood surrounding the horizon, which is not thermalized, with depth $\lambda_s$. Moreover, in our case, the 5-dim Schwarzschild radius is much smaller than $\lambda_s$, i.e. $r_{BH} = \frac{1}{2\pi T_{BH}} \ll \lambda_s$. This expression for the black hole radius $r_{BH}$ in terms of the temperature $T_{BH}$ is the 5-dim one. The radius and the area of the black hole that will be used in the estimations are given by \cite{41}

$$r_{BH} = \sqrt{\frac{8}{3\pi}} \frac{m_{BH}^{1/2}}{m_5^{3/2}}, \quad (6)$$

$$A_{BH} = 2\pi r_{BH}^3, \quad (7)$$

which are valid provided $r_{BH} \ll l$. The quantity $m_5$ is the 5-dim fundamental Planck
mass and \( l \) is the AdS radius. Due to the non-thermalization of the close neighborhood, the radiative particles propagate freely therein. This is why most particles radiated do not return to the black hole, and so, the flux of the Hawking radiation obeys the Stefan-Boltzmann’s law without corrections. The outer region that is thermalized [30] has as boundary the sphere with radius \( r_o = r_{BH} + \lambda_s \simeq \lambda_s \), which is a function of the local temperature \( T_o = \frac{\beta}{r_o} \). The radius \( r_o \) is the minimum thermalized radius and the temperature \( T_o \) is the boundary temperature.

Now we consider the transfer equation of the energy in the thermalized region to determine the temperature distribution \( T(r) \) assuming the diffusion approximation of photon transfer at the deep light-depth region [42]. The energy diffusion current in Local Temperature Equilibrium (LTE) is \( J_\mu = -\frac{\beta}{3T^3} \partial_\mu \rho \). In our case, the radiation density is \( \rho = \frac{\pi}{30} g^*_{SM} \beta^3 T^4(r) \), where \( g^*_{SM} = \sum f g^*_f = 106.75 \) is the massless freedom for all particles on the brane which is approximately equal to the massless freedom in SM. Also \( \beta/T \) is the effective MFP of all particles by all interactions on the brane with \( \beta \simeq 100 \). The transfer equation is \( \partial_\nu J_\mu = -\nabla_\mu J_\nu \). It is possible to find a stationary spherical-symmetric solution [42] which is

\[
T(r) = \left[ T_{br}^3 + (T_o^3 - T_{br}^3) \frac{r_o}{r} \right]^{1/3}.
\]

This solution assumes that the freedom of the massless particles \( g^*_{SM} \) is approximately constant which is valid up to all the interesting region of the domain wall. \( T_{br} = T(r \to \infty) \) is the background brane temperature. This temperature \( T_{br} \) is brane model dependent and it is related to the specific mechanism that created primordial black holes that dominated the universe. The value of \( T_{br} \) can be as large as a temperature somewhat lower that \( T_W \), where sphaleron rate is suppressed, and as low as zero. A very small \( T_{br} \) can be realized in a particular PBHs production model or in a scenario where the continuous accretion of PBHs made the background almost empty.

The outgoing diffusion flux is

\[
\mathcal{F} = 4\pi r^2 J(r) \simeq \frac{8\pi^3}{135} \beta_{s,3} g^*_{SM} [1 - (T_{br}/T_o)^3] T_o^2.
\]

This flux must be equal to the flux of the Hawking radiation

\[
\mathcal{F}_{BH} = 4\pi r_{BH}^2 \times \frac{\pi^2}{120} g^*_{SM} T_{BH}^4 + 2\pi^2 r_{BH}^3 \times \zeta g_{bulk} T_{BH}^5,
\]

where \( \zeta \) is a constant. The radiation towards the bulk can be neglected [39, 43] because the five-dimensional flux is negligible due to the small value of \( g_{bulk} \). The relation \( \mathcal{F}_{BH} = \mathcal{F} \) gives the temperature \( T_o \) of the minimum thermalized sphere with radius \( r_o \)

\[
r_o = \frac{16\pi}{3} \left( \frac{\beta^3 s}{\beta} \right)^{1/2} [1 - (T_{br}/T_o)^3]^{1/2} \frac{1}{T_{BH}}.
\]
and
\[ T_o = \frac{3}{16\pi \sqrt{\beta}} \left[ 1 - \left( \frac{T_{br}}{T_o} \right)^3 \right]^{-1/2} T_{BH}. \] (12)

Assuming that \( T_{br} \ll T_o \) the spherical thermal distribution surrounding the black hole is
\[ T(r) = \left( T_{br}^3 + \frac{9}{256\pi^2 \beta} \frac{T_{BH}^2}{r} \right)^{1/3} \] (13)
for \( r > r_o \).

Now we will discuss the formation of a domain wall around the black hole. A two-Higgs doublet model will be assumed since it is a quite general model that can include the supersymmetric Higgs sector. The symmetry is restored at the close neighborhood of the black hole because of its high temperature. At a greater distance, the temperature falls below the electroweak scale and the vacuum is broken. Therefore, an electroweak domain wall forms around the black hole, starting at radius \( r_{DW} \). The presented mechanism does not depend on the phase transition order and so it does not have to be first order. A second order transition, which is more favorite, has been adopted. The vacuum expectation value (vev) of Higgs doublets depends on the distance \( r \) from the center of the black hole.

The two-Higgs scalar potential can be written as follows [44]
\[ V_{\text{Higgs}} = \mu_1^2 \Phi_1^+ \Phi_1 + \mu_2^2 \Phi_2^+ \Phi_2 + \lambda_1 (\Phi_1^+ \Phi_1)^2 + \lambda_2 (\Phi_2^+ \Phi_2)^2 + \lambda_3 (\Phi_1^+ \Phi_1)(\Phi_2^+ \Phi_2) \\
+ \lambda_4 (\Phi_1^+ \Phi_2)(\Phi_2^+ \Phi_1) + \frac{1}{2} \lambda_5 [(\Phi_1^+ \Phi_2)^2 + (\Phi_2^+ \Phi_1)^2] + V_D, \] (14)
where \( \lambda_i \) are real numbers and \( \Phi_1^+ = (\phi_1 + i\phi_2, \phi_3 + i\phi_4), \Phi_2^+ = (\phi_5 + i\phi_6, \phi_7 + i\phi_8) \). Here, both the weak isospin doublets have weak hypercharge \( Y_{\text{weak}} = +1 \). We follow the notation of [44] in which both Higgs doublet fields have same hypercharge. The above potential, with the exception of \( V_D \) which we discuss in the following, is the most general one satisfying the following discrete symmetries
\[ \Phi_2 \rightarrow -\Phi_2, \quad \Phi_1 \rightarrow \Phi_1, \quad d_R^i \rightarrow -d_R^i, \quad u_R^i \rightarrow u_R^i, \] (15)
where \( u_R^i \) and \( d_R^i \) represent the right-handed weak eigenstates with charges \( \frac{2}{3} \) and \( -\frac{1}{3} \) respectively. All other fields involved remain intact under the above discrete symmetries. These symmetries force all the quarks of a given charge to interact with only one doublet. Thus, Higgs mediated flavour changing neutral currents are absent. If the discrete symmetry is broken during a cosmological phase transition, it produces stable domain walls via the Kibble mechanism [45]. This problem can be solved by adding terms which break
this symmetry, providing at the same time the required explicit CP violation for baryogenesis. The most general form of that part of the potential which breaks this discrete symmetry is

\[ V_D = -\mu_3^2 \Phi_1^\dagger \Phi_2 + \lambda_6 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + h.c. \]  

(16)

This is commonly named as \( D \)--breaking part. The parameters \( \mu_3 \), \( \lambda_6 \) and \( \lambda_7 \) are in general complex numbers

\[ \mu_3^2 = m_3^2 \, e^{i\theta_3}, \quad \lambda_6 = l_6 \, e^{i\theta_6}, \quad \lambda_7 = l_7 \, e^{i\theta_7}, \]  

(17)

providing explicit CP violation at the tree level.

In order to study the structure of the vacua we can perform an \( SU(2) \) rotation that sets the vev's of the fields \( \phi_{1,2,4} \) equal to zero. Solving the system \( \partial V_{\text{Higgs}} / \partial \phi_i = 0 \) implies several different stationary points. One of them is the usual asymmetric minimum that respects the \( U(1) \) of electromagnetism

\[ \Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ u \end{pmatrix}, \quad \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ ve^{i\varphi_t} \end{pmatrix}. \]  

(18)

In Eq. (18) \( u, v, \varphi_t \) are real numbers. The phase \( \varphi_t \) is the explicit CP violating angle at tree level that appears due to the existence of the \( D \)--breaking terms. The acceptable parameters of the model are those ensuring that the above stationary point becomes the absolute minimum at zero temperature.

In the cosmological context it is necessary to use the finite temperature effective potential. It is now known that most naturally the effective potential contains small cubic in temperature contribution, and thus, the phase transition is a second order one. After shifting the scalar fields about their expectation values the asymmetric minimum for the second doublet is

\[ \phi_{c,2} = \langle \phi_2(r) \rangle = v \, f(r) \, e^{i\varphi_t(T,r)}, \]  

(19)

where

\[ f(r) = \begin{cases} 0 & (r \leq r_{DW}) \\ \sqrt{1 - \left(\frac{T(r)}{T_w}\right)^2} & (r > r_{DW}) \end{cases} \]  

(20)

is a form-function of the wall and has a value from zero to one.

In order to define a width for our domain wall \( d_{DW} \) in this configuration of the Higgs vev, we have to define the value of \( f(r) \) at the end of the wall. Thus, we will introduce
a parameter $\xi$ that relates $d_{DW}$ with the radius of the symmetric region $r_{DW}$. Setting $T(r_{DW}) = T_W$ in Eq. (13), we find

$$d_{DW} = \xi r_{DW} = \xi \frac{9}{256\pi^2 \beta_{br}} \left[1 - \left(T_{br}/T_W\right)^3\right]^{-1} \frac{T_{BH}^2}{T_W^2}. \quad (21)$$

We are going to distinguish two cases: $\xi = 1$ which correspond to an end value $f = 0.6$, and $\xi = 10$ which correspond to an end value $f = 0.9$.

The structure of the electroweak domain wall is determined only by the thermal structure of the black hole and not by the dynamics of the phase transition as in the ordinary electroweak baryogenesis scenario (the CKN model). In the following subsections we are going to discuss two conditions ensuring that the LTE is valid. The first constraint is the size of the domain wall to be greater than the MFP, $1 < d_{DW}/\lambda_s(T_W)$. The second is the black-hole lifetime to be large enough to keep the stationary electroweak domain wall, $1 < \tau_{BH}/\tau_{DW}$. Both these constraints refer to the case without accretion. From now on we set $T_{br}$ practically zero, which is the most expected case.

### 3.1 First Constraint from Thermalization Condition without accretion

The stationary local thermal equilibrium assumption for the scalar wall is valid when the size of the wall is greater than the MFP. Thus, the first constraint is $1 < d_{DW}/\lambda_s(T_W)$, which gives

$$\left(\frac{3}{16\pi}\right)^2 \frac{\xi}{\beta_s \beta \gamma} \frac{T_{BH}^2}{T_W^2} > 1, \quad (22)$$

where $\gamma = 1 - (T_{br}/T_W)^3$. In the present study it is more important to find constraints on the black hole mass. Using further the modified formula for the mass of the black hole in five dimensions

$$m_{BH} = \frac{3}{32\pi} \frac{m_5^3}{T_{BH}^2}, \quad (23)$$

the equivalent constraint is

$$m_{BH} < \frac{\xi}{2} \left(\frac{3}{16\pi}\right)^3 m_5^3 T_W^{-2} (\beta_s \beta \gamma)^{-1}. \quad (24)$$

It is now easy to construct Table 1 with the allowed values of black hole masses for various values of the fundamental Planck scale.
| $m_5$     | $\xi = 1$          | $\xi = 10$       |
|-----------|-------------------|-----------------|
| 50 TeV    | $m_{BH} < 1.3$ TeV| $m_{BH} < 13$ TeV|
| 100 TeV   | $m_{BH} < 10.6$ TeV| $m_{BH} < 106$ TeV|
| 1000 TeV  | $m_{BH} < 1.06 \times 10^4$ TeV | $m_{BH} < 1.06 \times 10^5$ TeV|
| 5000 TeV  | $m_{BH} < 1.33 \times 10^6$ TeV | $m_{BH} < 1.33 \times 10^7$ TeV|
| 10000 TeV | $m_{BH} < 1.06 \times 10^7$ TeV | $m_{BH} < 1.06 \times 10^8$ TeV|

Table 1: Summary of the first constraint on the black hole mass for various values of $m_5$ and for the two domain wall thicknesses.

### 3.2 Second Constraint from BH Lifetime without accretion

The mean velocity of the outgoing diffusing particles at radius $r_{DW}$ is

$$v_{DW} = \frac{J(r_{DW})}{\rho(r_{DW})} = \left(\frac{32\pi}{9}\right)^2 \beta^2 \left[1 - (T_{br}/T_W)^3\right]^2 \left(\frac{T_W}{T_{BH}}\right)^2 .$$

The characteristic time scale for the construction of the stable electroweak domain wall \[30\] is

$$\tau_{DW} \simeq \frac{r_{DW}}{v_{DW}} = \frac{729}{262144\pi^4} \frac{1}{\beta_{br}^3 r_{r}^3 T_W^3} .$$

The black hole lifetime is needed to be estimated. Assuming that in the black hole dominated universe black holes are spatially separated enough to neglect accretion among them, we get \[39\]

$$\frac{dm_{BH}}{dt} \simeq -g_{*SM}\tilde{\sigma}_4 A_{eff,4} T^4 - g_{bulk}\tilde{\sigma}_5 A_{eff,5} T^5 ,$$

where $\tilde{\sigma}_4$ and $\tilde{\sigma}_5$ are the 4-dim and 5-dim Boltzmann constants per degree of freedom respectively, $A_{eff,4} = 4\pi r_{eff,5}^3$, $A_{eff,5} = 2\pi r_{eff,5}^3$, and $r_{eff,5} = 2r_{BH}$ is the effective black hole radius for black body emission. Neglecting now the evaporation to bulk \[43\], the black hole lifetime is

$$\tau_{BH} = t_{evap} \simeq \frac{1}{\tilde{\gamma}^{-1} l_4} \left(\frac{m_{BH}}{m_4}\right)^2 t_4 ,$$

where $m_4$ the 4-dim Planck mass, $l_4$ the 4-dim Planck length, $t_4$ the 4-dim Planck time and

$$\tilde{\gamma} \simeq \frac{1}{160} g_{*SM} + \frac{9\zeta(5)}{32\pi^4} g_{bulk} .$$

We have assumed that the degrees of freedom on the thermalised region of the brane are practically the same with the SM $g_{*SM} = 106.75$ because of the high temperature of the black hole, while $g_{bulk}$ is very small and can be ignored.
In order the mechanism to be viable the black hole lifetime should be larger than the
time for the domain wall construction. Thus, the second constraint $1 < \tau_{BH}/\tau_{DW}$ has to
be respected, which gives

$$m_{BH} > \tilde{g}^{1/4} \frac{6561^{1/4}}{2^7 \pi^{3/2}} (\beta \gamma)^{-3/4} m_5^{9/4} T_W^{-5/4}.$$  \hspace{1cm} (30)

This black hole mass refers to the initial black hole mass created, while $t_{\text{evap}}$ in Eq. (28)
is the time for the complete evaporation of this initial black hole mass. The bound of the
first constraint also refers to the initial black hole mass. The above constraint is the most
strict one. It can be naturally relaxed if the black hole is allowed to accrete plasma from
its neighborhood. This will be studied in next section.

For various values of the 5-dim Planck mass the black hole mass is bounded from
below, as shown in Table 2.

| $m_5$   | Black hole mass bound                  |
|---------|----------------------------------------|
| 50 TeV  | $m_{BH} > 42.9$ TeV                    |
| 100 TeV | $m_{BH} > 204$ TeV                     |
| 1000 TeV| $m_{BH} > 3.6 \times 10^4$ TeV         |
| 5000 TeV| $m_{BH} > 1.35 \times 10^6$ TeV        |
| 10000 TeV| $m_{BH} > 6.45 \times 10^6$ TeV       |

Table 2: Summary of the second constraint on the black hole mass for various values of
$m_5$.

### 3.3 Efficient Baryogenesis without accretion

Now we are going to estimate first the baryonic number created by a single black hole
and then the cosmic baryon to entropy ratio $b/s$. The demand $b/s \simeq 10^{-10}$ gives a strict
test for all baryogenesis mechanisms.

The sphaleron process works in all the symmetric region and the domain wall. However,
the baryon asymmetry production happens in the domain wall where both CP vi-
olation and non-equilibrium conditions exist. Futhermore, we want $f(r) = |\langle \phi_2(r) \rangle|/v \leq \epsilon = 1/100$ in order the exponential factor in the sphaleron process to be of order one
(otherwise the baryon asymmetry would be suppressed). This means that the effective
region of baryon generation is the region of the domain wall with small values of the Higgs scalar. The working region that produces baryons are from $r_{DW}$ till $r_{DW} + d_{sph}$. Then $d_{sph}$
is defined from $f(r_{DW} + d_{sph}) = \epsilon$. One now can see that
\[ \int_{r_{DW}}^{r_{DW} + d_{sph}} dr \frac{d}{dr} \varphi(r) = \epsilon \Delta \varphi_{CP} \]
where $\varphi(r, T) = [f(r) - 1] \Delta \varphi_{CP}$ [29]. Thus,
\[ \dot{B} = V \frac{\Gamma_{sph}}{T_W} N \dot{\varphi} \]
\[ = 4\pi N \kappa \alpha_W^5 T_W^3 r_{DW}^2 v_{DW} \int_{r_{DW}}^{r_{DW} + d_{sph}} dr \frac{d}{dr} \varphi(r) \]
\[ = \frac{1}{16\pi} N \kappa \alpha_W^5 \epsilon \Delta \varphi_{CP} \frac{T_{BH}^2}{T_W} \]
\[ = A T_{BH}^2, \quad (31) \]
where $\Gamma_{sph}$ is the sphaleron transition rate, $\Delta \varphi_{CP}$ the net CP phase, and it was set for convenience $A = \frac{1}{16\pi} N \kappa \alpha_W^5 \epsilon \Delta \varphi_{CP} \frac{1}{T_W}$. The black hole temperature can be expresses as a function of its lifetime [39]
\[ T_{BH} = \sqrt{\frac{3}{32\pi}} g^{-1/4} m_5^{3/4} t_{evap}^{-1/4}. \quad (32) \]
If we substitute $T_{BH}$ in Eq. (31) we get
\[ \dot{B} = A \frac{3}{32\pi} \dot{g}^{-1/2} m_5^{3/2} \tau_{BH}^{-1/2} \]
\[ = \tilde{A}(t_{evap,0} - t)^{-1/2}, \quad (33) \]
where $\tilde{A} = A \frac{3}{32\pi} \dot{g}^{-1/2} m_5^{3/2}$ and $t_{evap,0}$ is the time length for complete evaporation of the initial black hole mass. The time $t$ runs from 0 (black hole creation) to $t_{evap,0}$, and the baryon number created by a black hole in its lifetime is
\[ B = \int_0^{t_{evap,0}} \dot{B} dt \]
\[ = 2\tilde{A} t_{evap,0}^{1/2}. \quad (34) \]
Using Eq. (28) to substitute $t_{evap,0}$ in terms of the initial black hole mass $m_{BH}$, and $l/l_4 = (m_4/m_5)^3$ we find
\[ B = 2\tilde{A} \dot{g}^{-1/2} t_{4}^{1/2} \left( \frac{m_{BH}}{m_4} \right) \left( \frac{l}{l_4} \right)^{1/2} \]
\[ = 2\tilde{A} \dot{g}^{-1/2} m_5^{-3/2} m_{BH} \]
\[ = 3 \left( \frac{3}{16\pi} \right)^2 N \kappa \alpha_W^5 \dot{g}^{-1} T_W^{-1} \epsilon \Delta \varphi_{CP} m_{BH}. \quad (35) \]
Finally, the total baryon number density created from all black holes is $b = B n_{BH}$, where $n_{BH} = \frac{\rho_{BH}}{m_{BH}}$ is the number density of the black holes assuming a monochromatic spectrum of black holes.
In our scenario the universe is black hole dominated. Soon after the black holes complete evaporation, the universe is reheated. Therefore, the cosmic black hole density just before the final stage of very rapid evaporation is almost equal to the cosmic density radiation of the reheated plasma after the end of the evaporation

\[ \rho_{BH}(t_{reh}) \approx \rho_{rad}(t_{reh}) = \frac{\pi^2}{30} g_{reh} T_{reh}^4. \]  

(36)

The entropy density is given by

\[ s = \frac{9}{32 \pi^2} g_{reh} T_{reh}^3 \]  

where \( g_{reh} \) is the massless degrees of freedom of the reheated plasma in the asymmetric phase. We choose \( T_{reh} = 95 \) GeV in order to avoid the produced baryon asymmetry to be washed out (\( T_{reh} < T_W \approx 100 \) GeV). In our study there is the freedom to select the reheating temperature in contrast to the work \[30\], where mistakenly the reheating temperature was fixed using a wrong estimate of the black hole energy density. Thus, the baryon-to-entropy ratio is

\[ \frac{b}{s} = \frac{9}{(32 \pi)^2} N_{\kappa\ell W}^5 \tilde{g}^{-1} T_{reh} T_W \Delta \varphi_{CP}. \]  

(37)

Notice that the value of the baryon-to-entropy ratio depends neither to \( m_5 \) nor to \( m_{BH} \).

For some indicative values of \( \Delta \varphi_{CP} \) the baryon-to-entropy values are

\[ \Delta \varphi_{CP} = \pi \Rightarrow \frac{b}{s} = 1.2 \times 10^{-10} \]

\[ \Delta \varphi_{CP} = 0.1 \Rightarrow \frac{b}{s} = 4 \times 10^{-12}. \]  

(38)

The produced baryon-to-entropy value gets close to the observed \( b/s = 6 \times 10^{-10} \), but only for the maximum and not likely \( \Delta \varphi_{CP} = \pi \).

4 Baryogenesis and constraints with accretion

In this section we will investigate the role of accretion first to the successful and efficient baryogenesis and second to the realization of the existence of a black hole dominated era. We assume that black holes, after their formation, not only emit but also absorb radiation from their neighborhood. At the high energy regime of the RS universe, accretion is intense, and so, it is expected to result to a period that the whole density of the universe is equal or close to that of the black holes. Later on, during the cosmic evolution, evaporation starts to be more significant and finally the black holes annihilate, reheating the universe.

A phenomenological way to handle accretion is to introduce an effective factor \( f > 1 \) which denotes how much longer becomes the lifetime of the black hole

\[ \tau_{BH} = f \tilde{g}^{-1} m_5^{-3} m_{BH}^2. \]  

(39)
Now, the produced baryon number is modified to

\[ B = \frac{3f^{1/2}}{(16\pi)^2} N \kappa \alpha_5^5 \tilde{g}^{-1} T_w^{-1} \epsilon \Delta \varphi_{CP} m_{BH} \]  

(40)

and \( b/s \) of Eq. (37) is multiplied by \( f^{1/2} \). In order to have \( b/s \approx 6 \times 10^{-10} \), it must be

\[
\begin{align*}
\Delta \varphi_{CP} &= 1 \Rightarrow f \simeq 2 \times 10^2 \\
\Delta \varphi_{CP} &= 0.1 \Rightarrow f \simeq 2 \times 10^4 \\
\Delta \varphi_{CP} &= 0.01 \Rightarrow f \simeq 2 \times 10^6.
\end{align*}
\]

(41)

As it will be more clear below, such values of \( f \) can naturally be realised. This is a remarkable result. It is very easy to produce large values of baryon asymmetry and even larger than the required amount, for very small values of \( \Delta \varphi_{CP} \).

Let us discuss at this point the various constraints in the presence of accretion that extends the black hole lifetime. The first constraint Eq. (24) remains intact and refers to the maximum value of black hole mass reached just before the evaporation starts to dominate the accretion. However, the second bound is modified. It becomes less strict because the black hole lifetime is lengthened. The constrained black hole mass refers to the initial value of the black hole mass

\[ m_{BH,i} > f^{-1/4} \tilde{g}^{1/4} \frac{6561^{1/4}}{2^{7/2}} \frac{1}{(\beta \gamma)^3/4} m_5^{9/4} T_w^{-5/4}. \]

(42)

Table 3 shows some black hole mass bounds from below for some representative combinations of the involved free parameters.

In summary, taking into consideration both first and second constraint and demanding \( b/s \approx 6 \times 10^{-10} \), we can find allowed black hole mass ranges for various values of \( m_5 \) and \( \Delta \varphi_{CP} \), i.e. for \( m_5 = 50 \text{ TeV} \) and \( \Delta \varphi_{CP} = 0.01 \) the allowed range is \( 1.1 \text{ TeV} < m_{BH} < 13 \text{ TeV} \), for \( m_5 = 100 \text{ TeV} \) and \( \Delta \varphi_{CP} = 0.01 \) the allowed range is \( 5.3 \text{ TeV} < m_{BH} < 106 \text{ TeV} \), etc. These ranges differ from the previously mentioned case without accretion. There, the estimated ranges show the allowed range of the initial black hole mass. Here, in this section that accretion is added, the estimated ranges show the allowed wider possible range of the time dependent black hole mass during the accretion period. Thus, the range \( 5.3 \text{ TeV} < m_{BH} < 106 \text{ TeV} \) means that the initial black hole mass can be as low as 5.3 TeV and increases during accretion as large as 106 TeV. It is worth mentioning that for smaller values of CP, which is more favourable, the above allowed black hole mass ranges enlarge!
| $m_5$  | $f$                     | Initial black hole mass       |
|--------|-------------------------|--------------------------------|
| 50 TeV | $2 \times 10^4 (\Delta \varphi_{CP} = 1)$ | $m_{BH,i} > 11$ TeV           |
| 50 TeV | $2 \times 10^7 (\Delta \varphi_{CP} = 0.1)$ | $m_{BH,i} > 3.5$ TeV          |
| 50 TeV | $2 \times 10^9 (\Delta \varphi_{CP} = 0.01)$ | $m_{BH,i} > 1.12$ TeV         |
| 100 TeV| $2 \times 10^4 (\Delta \varphi_{CP} = 0.1)$ | $m_{BH,i} > 17$ TeV           |
| 100 TeV| $2 \times 10^9 (\Delta \varphi_{CP} = 0.01)$ | $m_{BH,i} > 5.3$ TeV          |

Table 3: Summary of the second constraint on the initial black hole mass for various values of $m_5$ and $f$. The values of $f$, $\Delta \varphi_{CP}$ are those that give the observed baryon asymmetry ratio.

In the RS model, there is a characteristic transition time $t_c$ that denotes the passage from the high-energy regime with the unconventional Hubble law to the low-energy regime. An interesting and workable case is when accretion is stronger than evaporation and continues till $t_c$, while afterwards evaporation is the dominant term in the differential equations. This case has been discussed in [39]. The black hole lifetime is

$$
\tau_{BH} = t_c + \tilde{g}^{-1} m_5^{-3} m_{BH,max}^2
= \frac{1}{2} \frac{m_4^2}{m_5^2} + \tilde{g}^{-1} m_{BH,max}^2
= \frac{1}{2} \frac{m_4^2}{m_5^2},
$$

(43)

where $m_{BH,max}$ is now the black hole mass at $t_c$. For $m_{BH,max} < m_4$, which is always the case in the present study, it is $\tau_{BH} \approx t_c$ and so the baryon number produced by a black hole becomes

$$
B = 2 \tilde{A} t_c^{1/2} = 2 A \frac{3}{32 \pi} \tilde{g}^{-1/2} m_5^{-3/2} t_c^{1/2}
= \frac{3}{\sqrt{2}} \frac{1}{(16 \pi)} \tilde{g}^{-1/2} N k \alpha_s \Delta \varphi_{CP} T W^{-1} m_4.
$$

(44)

Note that the final baryon to entropy ratio does not depend on $m_5$. Some indicative combinations of required CP angles and black holes masses ensuring $b/s \approx 6 \times 10^{-10}$ are

$$
m_{BH,max} = 10^4 TeV \Rightarrow \Delta \varphi_{CP} = 10^{-11}
m_{BH,max} = 10 TeV \Rightarrow \Delta \varphi_{CP} = 10^{-14}
m_{BH,max} = 1 TeV \Rightarrow \Delta \varphi_{CP} = 10^{-15}.
$$

(45)

The qualitative behaviour of the black hole mass time evolution is very sensitive on the accretion efficiency. If the efficiency is low, the dominant accretion stops inside the high energy regime and the above estimated $m_{BH,max}$ masses decrease.
Here, the first constraint remains the same and refers to the maximum black hole mass. On the other hand, the second constraint is practically always satisfied since now $t_c$ is very large, i.e. for $m_5 = 100$ TeV, $m_{BH} = 10$ TeV, we get $t_c/t_{evap} = 10^{29}$. The second constraint can be estimated from

$$t_{evap} + t_c > \tau_{DW} \iff m_{BH,i}^2 > \frac{729}{262144\pi^4} \frac{2}{\beta^3 \gamma^3} \left( \frac{3}{32\pi} \right)^2 \frac{m_5^6}{m_4^2 T_W^3}. \quad (46)$$

Since the accretion efficiency, the time at black hole formation, and initial black hole mass are unknown quantities, it is not useful to study quantitatively and fully various cases, solving the differential equation of black hole mass time evolution. However, it becomes apparent that successful baryogenesis can be achieved for very small values of CP angles, which can be provided also from different matter content than the two-Higgs model. Thus, our scenario does not depend on a specific form of the Higgs sector. It only requires a small CP angle on one scalar vev.

Note also that some of the evaporated baryon excess could be eaten from the same black hole during accretion. This phenomenon is expected not to be significant since the Hawking radiation has the escape velocity from the gravitational field. Another possibility is that some of the evaporated baryon asymmetric radiation to be eaten by nearby black holes. This complication becomes unimportant assuming that all black holes are initially widely separated while the expansion further increases the inter black holes distances.

### 4.1 Black hole domination era due to accretion

Let us discuss now the possibility of a black hole dominant era in the RS setup. This situation becomes easily realized due to the strong accretion at the high-energy regime. The differential equation that describes the black hole mass time evolution is

$$\frac{dm_{BH}}{dt} = F \pi r_{eff,5}^2 \rho_{rad} - g_{*SM} \frac{3 \Gamma (4) \zeta (4)}{2^6 \pi^4} \frac{m_5^3}{m_{BH}}, \quad (47)$$

where $F$ is the accretion efficiency and $\rho_{rad}$ is the energy density of the surrounding radiation.

According to the study in [39], if the accretion efficiency factor is $F > 0.78$, the PBH grows (accretion dominates evaporation) until $t_c$ is reached, provided the initial black hole mass is $m_{BH,i} > m_5$. If $F < 0.78$ then the loss due to evaporation is larger than the gain. There is also a case ($m_{BH,i} \gg m_5$ and low efficiency) where we have more accretion than
evaporation till “halt” time $t_h$ in the high-energy regime. In radiation dominated high-energy regime it can be proved that $t_h^{-1-q} \simeq q \left[ 1 + (1 - q) \frac{4\sqrt{\pi}}{g} \left( \frac{m_{\text{BH},i}}{m_5} \right)^{3/2} \right] t_i^{1-q}$, where $q = 4F/\pi$ and $\nu$ denotes what fraction of the horizon mass the initial black hole mass comprises.

Demanding a smaller evaporation than accretion, the second term in Eq. (47) becomes suppressed. The differential equation now takes the form

$$\frac{dm_{\text{BH}}}{dt} = \frac{2F}{\pi} \frac{m_{\text{BH}}}{t}$$

with solution $m_{\text{BH}} = m_{\text{BH},i}(t/t_i)^{2F/\pi}$. Let us assume the case where $\rho_{\text{rad}}$ initially, at the PBHs’ formation time $t_i$, is much higher than $\rho_{\text{BH}}$, i.e. $\rho_{\text{rad},i} = \mu_i n_{\text{BH}} m_{\text{BH},i}$ with $\mu_i > 1$. If at the end of accretion period at $t = t_f$ we have a black hole domination, then $\rho_{\text{rad},f} = \mu_f n_{\text{BH}} m_{\text{BH},i}(t_f/t_i)^{2F/\pi}$ with $\mu_f < 1$. Energy conservation implies

$$t_f = \left( \frac{1 + \mu_i}{1 + \mu_f} \right)^{\pi/2F} t_i.$$  \hspace{1cm} (49)

This expression implies that it is always possible to start with a radiation dominated era and end in a black hole dominated era within the high-energy regime. This holds since choosing a small enough value of $t_i$, the time duration $t_f$ can be smaller than $t_h$ or $t_c$, which is the upper bound for the dominant accretion period.

## 4.2 PBHs constraints

The model described in the present work should comply with the constraints coming from observational data. These constraints refer to the fraction at formation time of the mass of the universe going into PBHs, namely they refer to the quantity $\alpha_i = \frac{n_{\text{PBH}}}{n_{\text{tot}}}$, which is the upper bound for the dominant accretion period.

PBHs with masses below $10^4g$, the emitted photons from the evaporation do not violate the observed value of photon-to-baryon ratio. Supersymmetry or supergravity relics provide no limit on $\alpha_i$ for very small BH masses, so that the observed cold dark matter density is not exceeded. If PBH evaporations leave stable Planck-mass relics, these contribute to the dark matter, and in order not to exceed the critical density there arises an upper bound on $\alpha_i$, but for masses not as small as the ones here. In general, the analysis of all the above constraints has
been performed for the standard four-dimensional cosmology, so an appropriate analysis should consider the corresponding corrections due to extra dimensions. To conclude, all the constraints refer to four-dimensional PBHs with masses at least $10^{-5} g$ (created at Planck time $10^{-43} s$). Since our scenario is a higher-dimensional one with a fundamental mass scale of TeV, the allowed PBH masses are of this order, and therefore, it is quite probable that they are too small to be constrained by observational data.

Another general issue regarding accretion of matter into a black hole is the formation or not of shock waves subject to various conditions [52]. A shock is formed when the rotating flow has a high angular velocity that passes the centrifugal barrier. However, even if this velocity is somewhat lower, shocks can also be formed if the pressure of the flow is large. Most literature analyses semi-analytically and numerically this phenomenon in the context of astrophysical black holes. In addition, there are theoretical works assuming newtonian or post-newtonian physics that describe analytically the existence criteria of shock waves. Typically if the angular momentum $l$ is close to the marginally stable value and the initial kinetic energy $e$ for accretion or thermal energy for wind is within a few percent of the rest mass energy, the flow should pass through a shock. One major problem is that for a given set of $e$ and $l$ for every solution that includes a shock there exists another solution which is shock free. Numerical simulations show that if there are significant perturbations in the flow of falling material, more than a certain degree, then there is shock formation. However, these numerical works concern choice of parameters relevant for astrophysical black holes. For primordial black holes generated in a 4-dim FRW universe a crucial criterion is that the perturbation amplitude $\delta$ (defined as the relative mass excess inside the overdense region measured when it had the same scale as the cosmological horizon) is greater than a threshold value $\delta_c$. For perturbation with $\delta$ close to $\delta_c$, numerical calculations reveal that shocks are always formed.

In our context there are primordial black holes embedded in a surrounding cold radiation bath. The radiation temperature during the accretion period needs to be lower than the electroweak scale and it can be very much lower. However, this temperature depends on the specific cosmic scenario that creates the primordial black holes. It is reminded that the universe is reheated after the evaporation of all cosmic primordial black holes. Thus, the falling material needs not to have large kinetic energy. In addition, the fact that the accretion happens into the RS high energy regime makes the surrounding radiation plasma to be eaten more effectively contrary to the conventional FRW, as the expansion proceeds. The reason is that the slower decrease of the background density during the high-energy regime makes accretion important. Therefore the high energy
regime increases the accretion efficiency and not necessarily the speed of the rotating flow of falling material. Nevertheless, a complete study should consider i) the profile type of initial perturbations that created PBHs, ii) the five-dimensional geometry of the black holes, iii) the small black holes masses which make them hot enough to produce significant quantum evaporation, and iv) the complication that the escape of possible shock waves may feed the accretion of nearby black holes, depending on the inter black holes distances and the expansion rate. It worths investigating in a separate work for a certain cosmic scenario of production of brane primordial black holes, the possibility of the formation of shock waves during the accretion period. The study would almost certainly require numerical analysis.

Finally, let us finish mentioning one important point. Although we have performed our analysis of the BH accretion in the high energy regime of a RS cosmology, a similar analysis should also hold for any early cosmology with high energy modifications. Thus, alternative modified gravity models [53] or even braneworld models with high curvature corrections [54] should in principle equally well produce significant baryon asymmetry.

5 Black holes mass spectrum

In this section a discussion regarding the effects of a possible initial mass spectrum of primordial black holes is presented. Till now, a monochromatic mass spectrum was assumed. This was necessary in order to be able to find analytical expressions and inequalities and check first if the proposed baryogenesis mechanism works without any conflicts, and second if it is able to generate the required amount of baryon asymmetry.

Let us discuss how the various constraints on the black hole mass are affected from the existence of a black hole mass spectrum. The first constraint that ensures thermalization demands the size of the wall to be larger than the mean free path and this suggests an upper bound on the black hole mass. It is obvious that all the black holes of the spectrum with mass greater than this upper bound are not hot enough to thermalize the surrounding domain wall and thus they do not produce any baryon asymmetry. The exact distribution of the mass spectrum and its upper tail will determine how large or small a correction to the baryon asymmetry will be. It worths as a future work to adapt a specific mechanism of creation of primordial black holes and analyze numerically the proposed baryogenesis scenario. The second constraint, which comes from demanding the black hole lifetime to be larger than the time scale of stable domain wall construction, generates a lower bound on the black hole mass. Black holes smaller than this limit evaporate too soon. However,
as we have explained previously, this constraint in the presence of dominant accretion in the high energy regime becomes extremely weak, since the lifetime of small black holes is considerably extended.

Nevertheless, a not very narrow mass spectrum may modify the calculations of the produced baryon asymmetry. Indeed Eqs. (35), (40), (44) still hold, but now the total baryon number density created from all black holes is given from a more complicated expression

\[ b = \int_0^\infty B N(m, t)\,dm, \]  

with \( N \) the number density of the mass spectrum of black holes with masses between \( m \) and \( m + dm \). As a general conclusion it suffices to state that the very efficient baryogenesis due to accretion remains unaffected from the presence of mass spectrum. Based on a certain cosmological scenario of creation of PBHs one can estimate the exact baryon asymmetry straightforwardly. More details will follow concerning the relation of the black hole mass spectrum and the time evolution of the scale factor and the cosmic densities.

We are now going to obtain the equations that determine the evolution of the spectrum of primordial black holes, taking full account of either evaporation into radiation or accretion eating radiation, as well as the effect of the black holes on the evolution of the scale factor. It is assumed that the number density of the initial black hole spectrum is described by a power-law form, following [55], [56]. Thus, the initial number density of the primordial black hole spectrum between \( m_0 \) and \( m_0 + dm_0 \) is

\[ N(m_0)dm_0 = A m_0^{-n} \Theta(m_0 - m_c)\,dm_0 \]  

with \( m_0 = m(t = 0) \) the initial black hole mass. It has been assumed that all the black holes of the mass spectrum form simultaneously at a certain time otherwise analytic results become unnecessarily hard to be obtained. The \( \Theta \) function (with \( \Theta = 1 \) for \( x > 0 \) and \( \Theta = 0 \) for \( x \leq 0 \)) is introduced in order to model the presence of a cut-off mass in the spectrum and protects from the appearance of divergences at low masses limit. The cut-off mass \( m_c \) is natural to be a factor of the fundamental Planck mass, \( m_c = k m_p \), with \( k \) an arbitrary dimensionless constant. The power law should be such that the total energy density does not diverge at large masses and this implies \( n > 2 \). However, as Carr notes [55], initial density perturbations in FRW cosmologies that produce primordial black holes suggest values in the range \( 2 < n < 3 \). In RS cosmology similar ranges for the power law apply [19]. The constant \( A \) represents the amplitude of the spectrum and has appropriate units such that \( N(m_0)dm_0 \) is number density.
Next step is to determine analytically the spectrum $N(m,t)dm$. Both evaporation and accretion modify the value of the cut-off mass (evaporation reduces it). The number density at a given time will be

$$N(t) = \int_0^\infty N(m,t) \, dm, \quad (52)$$

while the energy density is given by

$$\varrho_{BH}(t) = \int_0^\infty N(m,t) \, m \, dm. \quad (53)$$

Since the purpose is to evaluate the modifications on the evolution of cosmic densities due to PBHs back-reaction, we are going to distinguish two cases. The first case concerns the description of the cosmic evolution after the evaporation starts to become dominant compared to the accretion. The second case is the description of the cosmic evolution during the era when accretion mainly determines the black hole mass evolution. Any attempt to seek analytical cosmological solutions considering both accretion and evaporation at the same time proved to be non fruitful. However, the most realistic scenario is this that comprises a long dominant accretion time period during the RS high energy regime which ends and is followed by a dominant evaporation era that results to a reheated radiation dominated universe.

### 5.1 Dominant evaporation era

First we will study the most interesting case when accretion has just stopped to be significant and evaporation dominates the evolution of the black hole mass. The significance of this analysis lies on finding the modifications on the expansion rate that have to be decreasing, allowing the emergence of the conventional radiation expansion law. Accretion has extended the black hole lifetime and thus significant baryogenesis has already been achieved. As soon as evaporation starts to dominate, something that is expected to be certainly true after the high energy regime $t > t_c$, the black hole mass rapidly decreases. The purpose is to estimate deviations on the cosmic densities and scale factor time evolutions.

The black hole mass spectrum has a time evolution first due to the expansion, which will be added later, and second and more physically important due to the evaporation. Denoting $m_{BH}$ by $m$ as above, the rate of loss of a single black hole is given by

$$\dot{m} = -g_{\nu\nu} \frac{m^3}{m}, \quad (54)$$
where
\[ g_{\text{tot}} = \frac{1}{2} \left[ \frac{0.0062}{G_{\text{brane}}} g_{*\text{SM}} + \frac{0.0031}{G_{\text{bulk}}} g_{\text{bulk}} \right] \simeq g_{*\text{SM}} \frac{3 \Gamma (4) \zeta (4)}{2^6 \pi^4} \]

and the second expression disregards the very small bulk contribution in \( g_{\text{tot}} \). The quantities \( G_{\text{brane}}, G_{\text{bulk}} \) represent the grey-body factors for brane and bulk respectively. In the standard cosmology the grey-body factor is equal to 2.6, but precise values are not well known for the braneworld, see discussion in [39]. The effective degrees of freedom \( g_{\text{tot}} \) is a function of temperature. For the time periods referring to the two cases we study in this section, we assume it is a constant. Eq. (54) can now be integrated and gives
\[ m^2 = m_0^2 - 2 g_{\text{tot}} m_5^3 t . \]

Solving Eq. (56) with respect to \( m_0 \) and differentiating, we are able to find the time evolution of the number density between \( m \) and \( m + dm \) at time \( t \). The time evolved spectrum is
\[ N(m, t) dm = A m^{-n} \left( 1 + \frac{2 g_{\text{tot}} m_5^3 t}{m^2} \right)^{-(n+1)/2} \Theta (m - m_{\text{cr}}(t)) dm , \]

where now the cut-off mass has also time evolved and is given by
\[ m_{\text{cr}}(t) = k m_5 \left( 1 - 2 g_{\text{tot}} k^{-2} m_5 t \right)^{1/2} . \]

It is obvious that after a time \( t_{\text{lim}} = \frac{k^2}{2 g_{\text{tot}} m_5} \) the cut-off mass reaches zero.

The energy per volume that is transferred from the black hole density to the radiation between times \( t \) and \( t + dt \) can be determined from Eq. (53) and is given by
\[ dE = \rho_{PH}(t) - \rho_{PH}(t + dt) = - \frac{\partial \rho_{BH}}{\partial t} dt . \]

The energy density rate can be estimated using the identity
\[ \frac{d}{dx} \int_{g(x)}^{f(x)} h(x, y) dy = \int_{g(x)}^{f(x)} \frac{\partial h(x, y)}{\partial x} dy + h(x, f(x)) \frac{df(x)}{dx} - h(x, g(x)) \frac{dg(x)}{dx} , \]

thus we find
\[ \frac{dE}{dt} = - \frac{d}{dt} \int_0^\infty N(m, t) m dm \]
\[ = A g_{\text{tot}} (n + 1) m_5^3 \int_{m_{\text{c, max}}}^\infty m^{-n-1} \left( 1 + \frac{2 g_{\text{tot}} m_5^3 t}{m^2} \right)^{-(n+3)/2} dm \]
\[ - A g_{\text{tot}} k^{-n} m_5^{-n+3} \left( 1 - 2 g_{\text{tot}} k^{-2} m_5 t \right) \Theta \left( \frac{k^2}{2 g_{\text{tot}} m_5} - t \right) , \]

23
where
\[ m_{c,\text{max}}(t) = \max[0, m_{cr}(t)]. \]  
(63)

The first term in Eq. (62) expresses the evolution of the spectrum and is the only non-zero term at late times. The second part of Eq. (62) arises due to the time evolution of the mass cut-off. It is apparent that for times larger than \( t_{\text{lim}} \) the lightest black holes completely evaporate and the \( \Theta \) function causes this term to vanish. Now it is possible to write the full equations of motion describing the expansion. We define for convenience the scale factor at \( t = 0 \) to be one, \( a(t = 0) = 1 \), where \( t = 0 \) corresponds to the time of primordial black holes formation. In all quantities calculated so far the dilution from expansion will have to be added, i.e. the spectral amplitude \( A \) becomes \( A a^{-3} \), the comoving density is \( \rho_{\text{BH}} = \rho_{\text{BH}} a^{-3} \), and the comoving energy is \( E_{\text{com}} = E a^{-3} \). Since the case under study concerns the dominant evaporation regime which most naturally starts after the high energy regime of the RS cosmology, the set of equations is the following

\[
\left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi}{3} m_{\text{4}}^2 (\rho_{\text{rad}} + \rho_{\text{BH}}) \tag{64}
\]

and

\[
\dot{\rho}_{\text{rad}} = -4 \frac{\dot{a}}{a} \rho_{\text{rad}} + \frac{dE_{\text{com}}}{dt}. \tag{65}
\]

Note that we have assumed that black holes exert unimportant kinetic pressure. Furthermore, for late times \( t > t_{\text{lim}} \)

\[
\rho_{\text{BH}} = \frac{1}{a^3} \int_0^{\infty} N(m, t) m \, dm = \frac{A}{a^3} \int_0^{\infty} m^{-n+1} \left( 1 + \frac{2g_{\text{tot}} m_{5}^3 t}{m^2} \right)^{-(n+1)/2} \, dm. \tag{66}
\]

It is convenient to set \( L = 2g_{\text{tot}} m_{5}^3 \) and \( \mu = \frac{m}{\sqrt{L} t} \). Now it is possible to estimate the integral

\[
\rho_{\text{BH}} = \frac{A}{a^3} \left( L t \right)^{-\frac{5}{n+2}} \int_0^{\infty} \mu^{-n+1} \left( 1 + \frac{1}{\mu^2} \right)^{-(n+1)/2} \, d\mu = \frac{A}{a^3} (2g_{\text{tot}} m_{5}^3 t)^{-\frac{5}{n+2}} \sqrt{\frac{\pi}{4}} \frac{\Gamma(-1 + \frac{n}{2})}{\Gamma(\frac{1 + n}{2})} , \tag{67}
\]

which holds for \( n > 2 \). We observe that it became possible to find the power of the time evolution of the black hole density \( \rho_{\text{BH}} \propto t^{-\frac{5}{n+2}} \). It depends on the spectral index \( n \) which most expectedly takes values \( 2 < n < 3 \). The comoving transfer rate per volume \( \frac{dE_{\text{com}}}{dt} \)
for $t > t_{\text{lim}}$ is given by

$$
\frac{dE_{\text{com}}}{dt} = \frac{A}{a^3} (n + 1) g_{\text{tot}} m_5^3 \int_0^{\infty} \frac{m^{-n-1} \left(1 + \frac{2 g_{\text{tot}} m_5^3}{m^2} t\right)^{-(n+3)/2}}{dm}
$$

$$
= \frac{A}{a^3} (L t)^{-n/2} (n + 1) g_{\text{tot}} m_5^3 \int_0^{\infty} \mu^{-n-1} \left(1 + \frac{1}{\mu^2}\right)^{-(n+3)/2} d\mu
$$

$$
= \frac{A}{a^3} (n + 1) (2 g_{\text{tot}} m_5^3)^{1/2} \sqrt{\frac{\pi}{8}} \frac{\Gamma\left(\frac{n}{2}\right)}{\Gamma\left(\frac{3+n}{2}\right)} t^{-\frac{n}{2}}.
$$

(68)

There are deviations in the time evolution of the radiation density compared to the conventional FRW model. Actually, Eq. (65) using (68) can be integrated to

$$
\rho_{\text{rad}} = \frac{c_0}{a^4} + \frac{c_1}{a^4} \int a t^{-n/2} dt
$$

where $c_0$ is an arbitrary constant and

$$
c_1 = A (n + 1) (2 g_{\text{tot}} m_5^3)^{1/2} \sqrt{\frac{\pi}{8}} \frac{\Gamma\left(\frac{n}{2}\right)}{\Gamma\left(\frac{3+n}{2}\right)}.
$$

(70)

Then, Eqs. (64), (67) give an integro-differential equation for the scale factor

$$
\left(\frac{\dot{a}}{a}\right)^2 = \frac{\tilde{c}_0}{a^4} + \frac{\tilde{c}_1}{a^4} \int a t^{-n/2} dt + \frac{\tilde{c}_2}{a^4} t^{2-n},
$$

(71)

where $\tilde{c}_0$ is an arbitrary constant and

$$
\tilde{c}_1 = \frac{8\pi}{3 m_4^2} c_1,
$$

(72)

$$
\tilde{c}_2 = \frac{8\pi}{3 m_4^2} A (2 g_{\text{tot}} m_5^3)^{1/2} \sqrt{\frac{\pi}{4}} \frac{\Gamma\left(-1 + \frac{n}{2}\right)}{\Gamma\left(\frac{1+n}{2}\right)}.
$$

(73)

Now, Eq. (71) can be converted, after a differentiation, into a Raychaudhuri equation

$$
2 a^3 H (2 H^2 + \dot{H}) = t^{-n/2} \left(\tilde{c}_1 + \tilde{c}_2 \frac{2-n}{2} + \tilde{c}_2 H t\right).
$$

(74)

The derived Raychaudhuri equation cannot be solved analytically but it can be shown that

$$
a \propto t^{1/2}
$$

is a solution of Eq. (74) neglecting terms of order $t^{-n/2}$. Thus, for times much after the end of evaporation the usual expansion is recovered. More definite results can be only extracted from numerical calculations and simulations covering various ranges of the involved free parameters.
5.2 Dominant accretion era

Here we will analyse another interesting case. It refers to the time period after primordial black hole creation. Since the creation happens in the high energy regime of RS cosmology it is expected accretion to be much more significant than evaporation. The purpose is to estimate the time evolutions of the cosmic densities and the scale factor.

The black hole mass spectrum has now a time evolution due to the accretion, apart from the expansion which will be added later. The rate of loss of a single black hole is given by

$$\dot{m} = F \pi r_{eff,5}^2 \rho_{rad} = F \frac{32}{3} m^3 \rho_{rad}, \quad (76)$$

where the $\rho_{rad}$ represents the surrounding to the black holes radiation density. The time duration of this case, where accretion is dominant, is much longer than the regime of dominant evaporation. Since most baryon asymmetry is produced during this accretion period it worths describing the complicated equations of motion. Eq. (76) can be solved and gives

$$m = m_0 \zeta \exp \left( \int_0^t \rho_{rad} \, dt \right), \quad (77)$$

where $\zeta = \exp \left( \frac{32 F}{3 m_5^3} \right)$.

Solving Eq. (77) with respect to $m_0$ and differentiating, we are able to find the time evolution of the number density between $m$ and $dm$ at time $t$, with the help of Eq. (51). The time evolved spectrum now is

$$N(m, t) dm = A \zeta^{n-1} \exp \left[ (n-1) \int_0^t \rho_{rad} \, dt \right] m^{-n} \Theta(m - m_{ca}(t)) \, dm, \quad (78)$$

where the cut off mass has been time evolved from $m_c$ to $m_{ca}$ given by

$$m_{ca}(t) = k m_5 \zeta \exp \left( \int_0^t \rho_{rad} \, dt \right). \quad (79)$$

It is obvious that contrary to the previous case the cut off mass does not equal zero at any time.

The energy per volume that is transferred from the eaten radiation to the black hole density between times $t$ and $t + dt$ can be determined from $dE = \varrho_{BH}(t) - \varrho_{BH}(t + dt) = -\frac{\partial \varrho_{BH}}{\partial t} \, dt$ and the energy density rate can be estimated using in addition Eq. (60). Thus

$$\frac{dE}{dt} = A \frac{n + 1}{n - 2} \zeta k^{-n+2} m_5^{-n+2} \exp \left( \int_0^t \rho_{rad} \, dt \right) \rho_{rad} \rho_{rad} \Theta(m - m_{ca}). \quad (80)$$

$$-A \zeta k^{-n+2} m_5^{-n+2} \exp \left( \int_0^t \rho_{rad} \, dt \right) \rho_{rad} \Theta(m - m_{ca}). \quad (81)$$

26
The first term in Eq. (80) expresses the evolution of the spectrum, while the second part arises due to the time evolution of the mass cut-off. In this second case this term does not vanish as long as evaporation is less significant than accretion. Now it is possible to write the full equations of motion describing the expansion. All densities should become comoving multiplying them with $a^{-3}$. In this case of dominant accretion regime we are clearly in the high energy regime of the RS cosmology. Therefore the set of equations is the following

$$
\left( \frac{\dot{a}}{a} \right)^2 = \frac{8\pi}{3m_4^2} \left( \rho_{\text{rad}} + \rho_{\text{BH}} + \frac{1}{2\lambda} (\rho_{\text{rad}} + \rho_{\text{BH}})^2 \right)
$$

with $\lambda = \frac{3m_6^6}{4\pi m_4^4}$ and

$$
\dot{\rho}_{\text{rad}} = -4\frac{\dot{a}}{a}\rho_{\text{rad}} + \frac{dE_{\text{cm}}}{dt}.
$$

For simplicity the same assumption as before has to be made, i.e. black holes exert unimportant kinetic pressure. Thus, we get

$$
\rho_{\text{BH}} = \frac{1}{a^3} \int_{m_{\text{ca}}}^{\infty} A \zeta^{n-1} \exp \left( (n-1) \int_0^t \rho_{\text{rad}} \, dt \right) m^{-n+1} \, dm
$$

$$
= \frac{A}{a^3} \frac{1}{n-2} \zeta (k m_5)^{-n+2} \exp \left( \int_0^t \rho_{\text{rad}} \, dt \right).
$$

We observe that in order to proceed further and be able to find the power of the time evolution of the black hole density we have to know the integral $\exp(\int_0^t \rho_{\text{rad}} \, dt)$ since $\rho_{\text{BH}}$ is proportional to it. The comoving transfer rate per volume $\frac{dE_{\text{cm}}}{dt}$ is given by

$$
\frac{dE_{\text{cm}}}{dt} = \frac{A}{a^3} \frac{n-1}{n-2} \zeta k^{-n+2} m_5^{-n+2} \rho_{\text{rad}} \exp \left( \int_0^t \rho_{\text{rad}} \, dt \right)
$$

$$
- \frac{A}{a^3} \zeta k^{-n+2} m_5^{-n+2} \rho_{\text{rad}} \exp \left( \int_0^t \rho_{\text{rad}} \, dt \right) \Theta(m - m_{\text{ca}}).
$$

The complete set of equations Eqs. (82), (83), (84) and (85) form an integro-differential system and can be solved only numerically for various ranges of the parameters.

6 Conclusions

The present study shows that the proposed baryogenesis scenario of accreting primordial black holes in a RS braneworld is capable to generate efficient baryogenesis even for very small CP violating angles. In summary the key points are

- The allowed by the mechanism BH mass range includes a mass spectrum around the higher dimensional Planck mass. The latter is important since this mass spectrum
is energetically favorable to be generated from high energy interactions in the very early braneworld cosmic history.

- The baryogenesis process in a 5-dim RS cosmology becomes easier than in the standard 4-dim universe because of the accretion in the high energy regime.

- The Higgs sector has not to be necessarily that of the two-Higgs model. It just requires a Higgs sector with very low CP asymmetry.

- It is not necessary the universe to be BH dominated at the time of the BHs creation since it is possible to turn into BH domination due to the accretion. However, since the proposed mechanism is able to generate very large baryon asymmetry, the black hole domination requirement is not crucial.

- The key point of producing large baryon asymmetry is the existence of an early high energy regime with an unconventional expansion rate that favors accretion. Thus, any alternative cosmological model bearing this feature can also give efficient baryogenesis.

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