Effect of Increase of Reinforcement Near Beam – Column Joints in Performance Based Design of Low-Rise Buildings

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Abstract: Due to its simplicity and capability in providing characteristic information that cannot be extracted via elastic static or dynamic analysis, the structural engineering profession has been using the non linear static procedure (NSP) or pushover analysis. Pushover analysis is carried out for either user defined nonlinear hinge properties or default – hinge properties, available in some programs based on the FEMA-356 and ATC-40 guidelines. The hinge properties depend upon the sectional properties of the columns / beam members. This paper studies the effect of increase of reinforcement of columns and beams near joints. Due to increase of reinforcement, the moment capacity of the non linear hinge will be increased which results in increase of the base shear capacity of the RCC building. Typical framed structure of 4 story, 5 story and 6 story are analyzed with increased joint reinforcement. Strong column and weak beam Principle is adopted while assuming sectional properties of the frame. The base shear versus displacements curves are compared. Considerable increase of base shear is observed when reinforcement in beams are increased. Very negligible increase of base shear is observed when reinforcement in column are increased.

Key words: Nonlinear Hinge, Pushover analysis, Base Shear Capacity.

I. INTRODUCTION

Since non linear behavior is intended in most structures subjected to earthquake loading, the use of non linear analysis is essential to capture the behavior of structures under seismic effects. The structural engineering profession has been using the non linear static procedure pushover analysis described in FEMA – 356 and ATC 40. It is widely accepted that, carefully used pushover analysis provides useful information that cannot be obtained by linear static or dynamic analysis procedures.

Modeling is one of the important steps in performing pushover analysis. The model has to consider the nonlinear behavior of the structure. The nonlinear properties of each component in the structure will contribute to the nonlinear behavior of the total structure. The nonlinear properties of the each component depends upon the plastic hinge properties / sectional properties of the members. In RCC framed structures , the hinge properties of the member depends up on the sectional properties and area of the reinforcement in concrete columns and beams. Based on the sectional properties of the member at the assumed location of hinge formation, the hinge properties will be generated in the well known nonlinear analysis software such as E-TABS and SAP etc.

If the same members have different sectional properties at different location, the hinge properties also will be changed along the length of the member. The deformation capacity of reinforced concrete structure depends upon the modeling assumptions.

This paper aims at study the effect of the increase of the reinforcement near beam and column joints on the base shear capacities of the total structure in performance based design. Three dimensional modeling is employed and E-TABS software programme is used for pushover analysis.
II. DESCRIPTION OF THE STRUCTURE:

Three structures i.e., four, five and six storied are considered to represent low-rise reinforced concrete building for study.

Properties of the Building:

Type of structure: Multi-storied moment resistance frame
Size of the Building: 24 m x 18 m
Number of stories: Three models consisting of 4, 5 and 6 storey
Height of Storey: 3 meters
Materials: Concrete M 25
Reinforcement: Fe 415
Wall thickness considered for load:
- External wall 230 mm
- Internal wall 115 mm
Size of column: 250 mm x 500 mm
Size of the beam: 250 mm x 400 mm
Depth of slab: 150 mm
Specific weight of the RCC: 25 KN/m³
Specific weight of the Wall: 20 KN/m³
Live Load: 3 KN/m²
Floor finish: 1 KN/m²

The Plan and Elevation are shown in the Fig.1 and Fig.2 Column reinforcement and Beam reinforcement are obtained as per elastic analysis without considering the seismic / wind forces and shown in Fig.3.

Fig.1 –Typical Plan of RCC Frame
Modeling approach:

Analysis have been performed using ETABS, which is a widely used structural design programme for static and dynamic analysis of the structures. A three dimensional model of each structure is created to carryout nonlinear statistic analysis. Beams and columns elements are modeled as nonlinear frame elements with plasticity by defining plastic hinges at both ends of column / beam members. The beam and column are divided into three parts i.e., central half part and quarter part on either side. The ¼ of the span of the beam and ¼th height of the column on either side of the beam &column joint are considered for strengthening by increase of reinforcement. The reinforcement in beams and column near joints for a length of 0.25 L is increased by 25%, 50% and 75% for each model for this study. The initial reinforcement in columns and beams is arrived based on the elastic analysis considering only gravity loads. The equivalent reinforcement is provided duly adopting selective combination of different dia of reinforcement bars. The % of increase is with reference to the initial reinforcement provided based on elastic analysis. The reinforcement provided in beams and columns is shown in Table I and II.
The nonlinear hinges are provided on either side of the quarter part and either side of the central half part of beams and columns to allow the failure mechanism in hinges in the central beam and column also, when reinforcement in members near joints is increased. Six Nos. of non linear hinges are provided for each column and beam as shown in figure 4.

ETABS implements the plastic hinge properties described in FEMA 356 (or ATC 40). The curve shown in figure 5 labeled A, B, C, D and E define the force-deformation behavior of plastic hinge. Where IO denotes Immediate Occupancy Level, LS denotes Limited Safety Level and CP denote Collapse Prevention level. The values assigned to each of these points vary depending up on the type of element, material properties, longitudinal and transverse steel content and the axial load Level on the element.

Fig. 4 – Hinge Location near Beam Column Joint

Fig. 5 – Force Deformation of a Typical Hinge
ETABS provides default hinge properties and considered PMM hinges for column and M3 hinges for beams. Once the structure is modeled with section properties, steel contents and the loads on it, defaults hinges properties (as per table 10.8 [6]) will be assigned to the members.

The default hinge properties of the beam depends upon the ratio of $\frac{P_{p} - P_{p'}}{P_{bal}}$, $\frac{V}{b_{w}d}$ and column depends up on the ratio of $\frac{P}{A_{q}f_{c}}$, $\frac{A_{v}}{b_{w}d}$ where as

$p = \text{Ratio of tension reinforcement, } P_{bal} = \text{Reinforcement ratio producing balanced strain conditions, } P' = \text{Ratio of compression reinforcement, } V = \text{Design shear force at section concurrent with moment, } b_{w} = \text{Web width, } d = \text{Distance from extreme compression fiber to centroid of tension reinforcement, } f_{c} = \text{Compression strength of concrete, } P = \text{Axial force in concrete column, } A_{g} = \text{Gross area of the column, } s = \text{Spacing of shear reinforcement.}$

The non linear hinge properties of the beam depend up on longitudinal and transverse reinforcement and where as the non linear hinge properties of the column depend up the transverse reinforcement only. It is assumed that the shear reinforcement confirms the required spacing provision in modeling the non linear hinge prosperities.

**Pushover analysis:**

The push over analysis consists of the application of gravity loads and representative lateral load pattern. The building is subjected to gravity loading and simultaneous lateral loading.

There are sixteen models generated for each 4 stories, 5 stories and 6 stories buildings. One of it is the basic model with required reinforcement for gravity loading and other fifteen models are with combination of changes in the beam and column reinforcement i.e., 25%, 50% and 75% increase. The pushover curve for displacement in ‘x’ direction and ‘y’ direction verses base shear are obtained.

**Table – I. (Longitudinal Reinforcement provided in Beam)**

| Area increased by | 4 storey | 5 storey | 6 storey |
|-------------------|----------|----------|----------|
|                   | Top      | Bottom   | Top      | Bottom   | Top      | Bottom   |
| 0%                | 2 Nos. 16 Dia  | 2 Nos. 16 Dia  | 2 Nos. 16 Dia  | 2 Nos. 16 Dia  | 2 Nos. 16 Dia  | 2 Nos. 16 Dia  |
| 25%               | 2 Nos. 16 Dia + 1 No. 12 Dia  | 2 Nos. 16 Dia + 1 No. 12 Dia  | 2 Nos. 16 Dia + 1 No. 12 Dia  | 2 Nos. 16 Dia + 1 No. 12 Dia  | 2 Nos. 16 Dia + 1 No. 12 Dia  | 2 Nos. 16 Dia + 1 No. 12 Dia  |
| 50%               | 3 Nos. 16 Dia  | 3 Nos. 16 Dia  | 3 Nos. 16 Dia  | 3 Nos. 16 Dia  | 3 Nos. 16 Dia  | 3 Nos. 16 Dia  |
| 75%               | 2 Nos. 16 Dia + 1 No. 20 Dia  | 2 Nos. 16 Dia + 1 No. 20 Dia  | 2 Nos. 16 Dia + 1 No. 20 Dia  | 2 Nos. 16 Dia + 1 No. 20 Dia  | 2 Nos. 16 Dia + 1 No. 20 Dia  | 2 Nos. 16 Dia + 1 No. 20 Dia  |

**Table – II. (Longitudinal Reinforcement provided in Columns )**

| Area increased by | 4 storey | 5 storey | 6 storey |
|-------------------|----------|----------|----------|
|                   | All floors | All floors | Column base and ground floor | Other floors |
|                   | All Columns | All Columns | External Columns | Internal Columns | All Columns |
| 0%                | 4 Nos. 12 Dia + 4 Nos. 14 Dia  | 4 Nos. 12 Dia + 4 Nos. 14 Dia  | 4 Nos. 12 Dia + 4 Nos. 16 Dia  | 4 Nos. 16 Dia + 4 Nos. 20 Dia  | 4 Nos. 12 Dia + 4 Nos. 14 Dia  |
| 25%               | 4 Nos. 12 Dia + 4 Nos. 16 Dia  | 4 Nos. 12 Dia + 4 Nos. 16 Dia  | 4 Nos. 12 Dia + 4 Nos. 18 Dia  | 8 Nos. 20 Dia  | 4 Nos. 12 Dia + 4 Nos. 16 Dia  |
| 50%               | 4 Nos. 12 Dia + 4 Nos. 18 Dia  | 4 Nos. 12 Dia + 4 Nos. 18 Dia  | 4 Nos. 14 Dia + 4 Nos. 20 Dia  | 4 Nos. 18 Dia + 4 Nos. 26 Dia  | 4 Nos. 12 Dia + 4 Nos. 18 Dia  |
| 75%               | 4 Nos. 16 Dia + 4 Nos. 18 Dia  | 4 Nos. 16 Dia + 4 Nos. 18 Dia  | 4 Nos. 16 Dia + 4 Nos. 20 Dia  | 4 Nos. 20 Dia + 4 Nos. 26 Dia  | 4 Nos. 16 Dia + 4 Nos. 18 Dia  |
### III. RESULTS AND DISCUSSIONS

The three Models 4, 5 and 6 storey are analyzed by using “ETABS”software and the results i.e., the maximum displacement versus base shear values are tabulated as below.(Table III to Table VIII)

#### Table – III. (4 storey Building)

| Type of Reinforcement | Deflection in “X” direction (in mm) | Base Shear in “X” direction (in KN) | Deflection in “Y” direction (in mm) | Base Shear in “Y” direction (in KN) |
|-----------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| 4SB1.00 C 1.00        | 118.023                           | 50813.38                          | 32.46                             | 43594.75                          |
| 4SB1.00 C 1.25        | 132.62                            | 51498.75                          | 32.46                             | 43594.75                          |
| 4SB1.00 C 1.50        | 129.10                            | 52081.61                          | 32.46                             | 43594.75                          |
| 4SB1.00 C 1.75        | 148.56                            | 52605.62                          | 44.74                             | 44110.97                          |
| 4SB1.25C 1.00         | 102.45                            | 55620.59                          | 41.48                             | 52587.67                          |
| 4SB1.25 C 1.25        | 116.27                            | 56322.11                          | 83.63                             | 54276.53                          |
| 4SB1.25 C 1.50        | 138.11                            | 57101.32                          | 88.77                             | 54877.39                          |
| 4SB1.25 C 1.75        | 140.42                            | 57621.57                          | 95.72                             | 55303.80                          |
| 4SB1.50 C 1.00        | 90.70                             | 59353.69                          | 64.33                             | 57080.79                          |
| 4SB1.50 C 1.25        | 109.69                            | 60025.50                          | 64.94                             | 57487.37                          |
| 4SB1.50 C 1.50        | 120.87                            | 60697.49                          | 77.70                             | 58288.97                          |
| 4SB1.50 C 1.75        | 122.88                            | 61293.82                          | 81.51                             | 58920.08                          |
| 4SB1.75C 1.00         | 98.46                             | 62892.96                          | 54.18                             | 60877.53                          |
| 4SB1.75C 1.25         | 95.96                             | 64356.10                          | 58.995                            | 61281.61                          |
| 4SB1.75C 1.50         | 105.84                            | 65255.85                          | 60.169                            | 61983.98                          |
| 4SB1.75C 1.75         | 114.16                            | 65798.69                          | 73.53                             | 62632.60                          |

#### Table – IV. (5 storey Building)

| Type of Reinforcement | Deflection in “X” direction (in mm) | Base Shear in “X” direction (in KN) | Deflection in “Y” direction (in mm) | Base Shear in “Y” direction (in KN) |
|-----------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| 5SB1.00 C 1.00        | 134.63                            | 57316.90                          | 54.26                             | 53580.46                          |
| 5SB1.00 C 1.25        | 120.50                            | 57180.69                          | 43.87                             | 53388.01                          |
| 5SB1.00 C 1.50        | 173.06                            | 57849.04                          | 42.52                             | 51102.52                          |
| 5SB1.00 C 1.75        | 174.80                            | 58105.19                          | 32.06                             | 47401.72                          |
| 5SB1.25 C 1.00        | 146.13                            | 62477.24                          | 72.91                             | 62396.30                          |
| 5SB1.25 C 1.25        | 141.31                            | 63181.46                          | 79.13                             | 62910.72                          |
| 5SB1.25 C 1.50        | 143.11                            | 63905.40                          | 84.26                             | 63447.76                          |
| 5SB1.25 C 1.75        | 154.52                            | 64267.79                          | 82.30                             | 63924.08                          |
| 5SB1.50 C 1.00        | 132.01                            | 66262.40                          | 67.07                             | 66606.98                          |
| 5SB1.50 C 1.25        | 143.46                            | 67281.29                          | 72.81                             | 66968.83                          |
| 5SB1.50 C 1.50        | 152.07                            | 68148.33                          | 66.40                             | 67394.66                          |
| 5SB1.50 C 1.75        | 146.41                            | 68502.80                          | 84.38                             | 67908.76                          |
| 5SB1.75 C 1.00        | 101.37                            | 69988.04                          | 55.68                             | 71248.80                          |
| 5SB1.75 C 1.25        | 112.69                            | 70713.57                          | 62.61                             | 71962.60                          |
| 5SB1.75 C 1.50        | 156.19                            | 72885.58                          | 67.70                             | 72260.25                          |
| 5SB1.75 C 1.75        | 159.23                            | 73088.15                          | 71.61                             | 72482.51                          |
### Table V. (6 storey Building)

| Type of Reinforcement | Deflection in “X” direction (in mm) | Base Shear in “X” direction (in KN) | Deflection in “Y” direction (in mm) | Base Shear in “Y” direction (in KN) |
|-----------------------|-------------------------------------|-------------------------------------|-------------------------------------|-------------------------------------|
| 6SB1.00 C 1.00        | 185.00                              | 65061.34                            | 64.59                               | 63361.22                            |
| 6SB1.00C 1.25         | 188.27                              | 65672.70                            | 41.88                               | 58469.58                            |
| 6SB1.00C 1.50         | 3.379                               | 13696.60*                           | 4.62                                | 18189.62*                           |
| 6SB1.00C 1.75         | 11.227                              | 24984.18*                           | 12.747                              | 22111.94*                           |
| 6SB1.25C 1.00         | 112.29                              | 69372.91                            | 62.63                               | 72535.61                            |
| 6SB1.25 C 1.25        | 187.44                              | 71752.76                            | 73.53                               | 72934.49                            |
| 6SB1.25C 1.50         | 9.86                                | 21977.59*                           | 11.24                               | 19539.43*                           |
| 6SB1.25C 1.75         | 11.227                              | 24984.18*                           | 12.747                              | 22111.94*                           |
| 6SB1.50C 1.00         | 173.64                              | 75121.23                            | 51.24                               | 74364.43                            |
| 6SB1.50C 1.25         | 185.38                              | 76151.11                            | 50.53                               | 74564.46                            |
| 6SB1.50C 1.50         | 9.86                                | 21977.59*                           | 11.24                               | 19539.43*                           |
| 6SB1.50C 1.75         | 11.227                              | 24984.18*                           | 12.75                               | 22111.94*                           |

Note: * Due to non-convergence of the iteration process, the required results could not be obtained and these values are not considered in analysis.

### Table VI. (Increase of Base Shear for Increase of Reinforcement in Columns)

| % increase in reinforcement | Model No. | % increase in base shear (X-Direction) | % increase in base shear (Y-Direction) |
|-----------------------------|-----------|---------------------------------------|---------------------------------------|
| 25                          | 4SB1.00 C 1.25 | 1.35                                  | 0                                     |
|                             | 5SB1.00 C 1.25 | 0                                     | 0                                     |
|                             | 6SB1.00 C 1.25 | 0.94                                  | 0                                     |
| 50                          | 4SB1.00 C 1.50 | 2.50                                  | 0                                     |
|                             | 5SB1.00 C 1.50 | 0.93                                  | 0                                     |
|                             | 6SB1.00 C 1.50 | 0                                     | 0                                     |
| 75                          | 4SB1.00 C 1.75 | 3.53                                  | 1.18                                  |
|                             | 5SB1.00 C 1.75 | 1.38                                  | 0                                     |
|                             | 6SB1.00 C 1.75 | -                                     | -                                     |

### Table VII. (Increase of Base Shear for Increase of Reinforcement only in Beams)

| % increase in reinforcement | Model No. | % increase in base shear (X-Direction) | % increase in base shear (Y-Direction) |
|-----------------------------|-----------|---------------------------------------|---------------------------------------|
| 25                          | 4SB1.25 C 1.00 | 9.46                                  | 20.63                                 |
|                             | 5SB1.25 C 1.00 | 9.00                                  | 16.45                                 |
|                             | 6SB1.25 C 1.00 | 6.63                                  | 14.48                                 |
| 50                          | 4SB1.50 C 1.00 | 16.81                                 | 30.94                                 |
|                             | 5SB1.50 C 1.00 | 15.61                                 | 24.31                                 |
|                             | 6SB1.50 C 1.00 | 15.46                                 | 17.37                                 |
| 75                          | 4SB1.75 C 1.00 | 25.74                                 | 39.64                                 |
|                             | 5SB1.75 C 1.00 | 22.00                                 | 32.98                                 |
|                             | 6SB1.75 C 1.00 | 23.06                                 | 17.67                                 |
Table – VIII. (Increase of Base Shear for Increase of Reinforcement in Both Columns and Beams)

| % increase in reinforcement | Model No.       | % increase in base shear (X-Direction) | % increase in base shear (Y-Direction) |
|-----------------------------|-----------------|----------------------------------------|----------------------------------------|
| 25                          | 4SB1.25 C 1.25  | 10.84                                  | 24.5                                   |
| 5SB1.25 C 1.25              |                 | 10.23                                  | 17.41                                  |
| 6SB1.25 C 1.25              |                 | 10.28                                  | 15.11                                  |
| 50                          | 4SB1.50 C 1.50  | 19.45                                  | 33.71                                  |
| 5SB1.50 C 1.50              |                 | 18.90                                  | 25.78                                  |
| 6SB1.50 C 1.50              |                 | -                                      | -                                      |
| 75                          | 4SB1.75 C 1.75  | 29.49                                  | 43.67                                  |
| 5SB1.75 C 1.75              |                 | 27.52                                  | 35.28                                  |
| 6SB1.75 C 1.75              |                 | -                                      | -                                      |

Monitored Displacement in mm

Fig 6 - PUSHOVER CURVE IN X-DIRECTION - 4 STOREY

Fig 7 - PUSHOVER CURVE IN Y-DIRECTION - 4 STOREY
Fig 8 - PUSH OVER CURVE IN X-DIRECTION - 5 STOREY

Fig 9 - PUSH OVER CURVE IN Y DIRECTION - 5 STOREY

Fig 10 - PUSH OVER CURVE IN X DIRECTION - 6 STOREY
Fig 11 - PUSH OVER CURVE IN Y DIRECTION - 6 STOREY

Fig 12 - PUSH OVER CURVE IN X DIRECTION - 0% INCREASE IN REINFORCEMENT NEAR JOINTS

Fig 13 - PUSH OVER CURVE IN Y DIRECTION - 0% INCREASE IN REINFORCEMENT NEAR JOINTS
Fig 14 - PUSH OVER CURVE IN X-DIRECTION - 25% INCREASE IN REINFORCEMENT NEAR JOINTS

Fig 15 - PUSH OVER CURVE IN Y-DIRECTION WITH 25% INCREASE IN REINFORCEMENT NEAR JOINTS
Fig 16 - PUSH OVER CURVE IN X-DIRECTION - 50% INCREASE IN REINFORCEMENT NEAR JOINTS

Fig 17 - PUSH OVER CURVE IN Y-DIRECTION - 50% INCREASE IN REINFORCEMENT NEAR JOINTS

Fig 18 - PUSH OVER CURVE IN X-DIRECTION - 75% INCREASE IN REINFORCEMENT NEAR JOINTS
The following observations are made from the results obtained.

1) The base shear capacity of the RCC building is considerably increased by increasing the reinforcement in beams near beam-column joints.

2) (a) The base shear capacity of the building in ‘X’ direction is increased up to 30% by increase of 75% reinforcement in beams and columns near joints. The increase is reduced gradually from 4th story to 6 story building.
   (b) The base shear capacity of the building in ‘Y’ direction is increased up to 43%. The increase is reduced gradually from 4th and 6th story.

3) (a) The base shear capacity in ‘x’ direction is increased up to 25% for increase of 75% of only beam reinforcement.
   (b) The base shear capacity in ‘y’ direction is increased up to 39% for increase of 75% only beam reinforcement near joints.

4) The increase of base shear capacity in both ‘X’ and ‘Y’ direction is very negligible when only column reinforcement is increased.

5) In general the increase in base shear capacity in ‘Y’ direction is more than comparative to the increase in X directions.
   It may be mainly due to the more stiffness of the building in ‘X’ direction when comparative to the ‘Y’ direction.

The reasons for the negligible increase in base shear capacity when only column reinforcement near joints is increased may be due to the fact that

(i) The model is designed such that strong column and weak beam principle is followed.
(ii) The hinge properties of the column do not depend on the longitudinal reinforcement of the column

IV. CONCLUSIONS

1) The increase in the reinforcement in column joints has negligible impact in base shear capacity of the building.

2) The increase in the reinforcement of beam joints has substantial impact on the base shear capacity for the low rise buildings (4 to 6 stories which are commonly adopted).

3) The increase in base shear capacity in Y direction (weaker direction) is more.

4) The increase in base shear capacity due to increase of reinforcement at joints is slightly decreasing with increase of number of floors.

5) The seismic design of low rise buildings for severe earthquake zone also can be more economically designed by this performance based nonlinear static pushover analysis method.
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