Phase Transformations in the High-$T_c$ Superconducting Compounds, Ba$_2$RCu$_3$O$_{7-\delta}$ ($R=$Nd, Sm, Gd, Y, Ho, and Er)

The phase transformation between the orthorhombic and tetragonal structures of six high-$T_c$ superconductors, Ba$_2$RCu$_3$O$_{7-\delta}$, where $R=$ Nd, Sm, Gd, Y, Ho, and Er, and $\delta=0$ to 1, has been investigated using techniques of x-ray diffraction, differential thermal analysis/thermogravimetric analysis (DTA/TGA) and electron diffraction. The transformation from the oxygen-rich orthorhombic phase to the oxygen-deficient tetragonal phase involves two orthorhombic phases. A superlattice cell caused by oxygen ordering, with $a'=2a$, was observed for materials with smaller ionic radius (Y, Ho, and Er). For the larger lanthanide samples (Nd, Sm, and Gd), the $a'=2a$ type superlattice cell was not observed.

The structural phase transition temperatures, oxygen stoichiometry and characteristics of the $T_c$ plateaus appear to correlate with the ionic radius, which varies based on the number of f electrons. Lanthanide elements with a smaller ionic radius stabilize the orthorhombic phase to higher temperatures and lower oxygen content. Also, the superconducting temperature is less sensitive to the oxygen content for materials with smaller ionic radius. The trend of dependence of the phase transformation temperature on ionic radius across the lanthanide series can be explained using a quasi-chemical approximation (QCA) whereby the strain effect plays an important role on the order-disorder transition due to the effect of oxygen content on the CuO chain sites.

Key words: ac magnetic susceptibility; orthorhombic/tetragonal transformation; oxygen ordering; phase transformation of Ba$_2$RCu$_3$O$_{7-\delta}$ ($R=$lanthanides); strain effect on phase transition; transition temperature.

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both film deposition and open-air solution techniques [14-22]. To further optimize the superconducting properties of long-length coated conductors for practical applications, recent research has also included the use of lanthanide-substituted variants, Ba$_2$R$_2$Cu$_3$O$_{7-\delta}$ (R=lanthanides with stable 3+ oxidation state). Phase equilibrium research pertaining to Ba$_2$RCu$_3$O$_{7-\delta}$, including a thorough understanding of phase transition phenomena, is therefore important for processing.

The progressive reduction in size of the lanthanide, which is known as the lanthanide contraction, allows systematic study of the trend of crystal chemistry, solid solution formation, and phase equilibria in the systems BaO-R$_2$O$_3$-CuO as a function of the size of lanthanide ion, R$^{3+}$ [23-29]. Numerous investigations pertaining to the crystal chemistry, and the effect of oxygen stoichiometry on properties of Ba$_2$RCu$_3$O$_{7-\delta}$ have been reported [30-35]. The present paper is part of our continuing effort to understand the effect of lanthanide substitution on the properties and processing parameters of the high-$T_c$ superconductors Ba$_2$RCu$_3$O$_{7-\delta}$ [23-29,36-39]. Since our preliminary reports [36-38] on the structural phase transitions of Ba$_2$RCu$_3$O$_{7-\delta}$ for R = Sm, Gd, Er, Y, and Ho, we have completed studies of the Nd series, including additional characterization of some of these materials using electron diffraction techniques. We have also improved our understanding of the phase transition in Ba$_2$RCu$_3$O$_{7-\delta}$ as related to the size of ionic radius of R$^{3+}$ by using a quasi-chemical approximation to describe the effect of oxygen disorder [40].

After annealing the Ba$_2$RCu$_3$O$_{7-\delta}$ compounds at various temperatures and then rapidly quenching to liquid nitrogen temperature, we have made several observations concerning the phase transitions in these materials. Most interesting is the presence of $T_c$ plateaus (annealing temperature ranges over which $T_c$ remains approximately constant, even as the oxygen content changes). Examples are given of the existence of a 90 K and a 60 K $T_c$ plateau in the Y, Ho, and Er materials [36-38,41-42]. Although there are extensive literature reports [43-49] describing the experimental observations or theoretical predictions of a single phase 60 K material in the Y system, very little information has previously been reported describing the lanthanide-substituted materials. Furthermore, most of the reported Y materials were prepared using processing routes different from our quenching methods [46-49].

2. Experimental

Since Nd$_2$O$_3$ reacts with atmospheric moisture to form Nd(OH)$_3$, the Nd$_2$O$_3$ powder was heat-treated at 600 °C overnight prior to sample preparation. A single phase master batch of Ba$_2$NdCu$_3$O$_{7-\delta}$ was prepared from a stoichiometric mixture of CuO, Nd$_2$O$_3$ and BaCO$_3$. Before firing and annealing, the powder was pressed into pellets and placed on MgO single crystals. The pellets were reground and annealed several times until the presence of a single-phase material was confirmed by x-ray powder diffraction analysis. Annealing was carried out at temperatures of 850 °C, 870 °C, and 900 °C each in air for 1 d, followed by firing in air at 940 °C for 2 d. Analysis by scanning electron microscopy and energy dispersive x-ray analysis (SEM/EDS) showed absence of substitution of magnesium in these samples.

A total of 10 barium-neodymium-copper-oxide samples were prepared for this investigation from the single-phase master batch. Batches of the other Ba$_2$RCu$_3$O$_{7-\delta}$ phases were prepared in similar fashion, using the appropriate lanthanide oxides [36-38]. To investigate the phase transitions, specimens weighing about 200 mg to 500 mg were annealed in an MgO crucible for up to 2 d in air at temperatures between 400 °C and 900 °C. The temperature was measured using a Pt/Pt10Rh thermocouple calibrated against the melting point of gold. Temperature of the Pt-wound resistance furnace used in these experiments was controlled to ±2 °C by using a Wheatstone bridge type controller. After annealing, the samples were quenched into a liquid nitrogen-cooled copper cold well, through which liquid nitrogen-cooled helium gas was passed at a rapid rate (Fig. 1). Rapid cooling under these conditions prevented the oxygen gain that would normally occur for samples cooled in air.

Samples studied by electron microscopy are listed in Table 1, together with their processing conditions and oxygen content (all were quenched in liquid nitrogen-cooled helium). Specimens for electron microscopy were prepared by crushing small pieces of the sample material and then following one of two procedures: either the powder was dispersed in ethanol and drops of the liquid were placed on a carbon-coated copper grid, or a grid was scooped through the powder to avoid possible reactions with the alcohol. These two techniques produced samples with no detectable differences between them. Conventional electron microscopy and electron diffraction were carried out at 120 keV and 300 keV, and exposure times up to 50 s were used to record the faint superlattice diffraction spots.
The oxygen content of the Ba$_2$RCu$_3$O$_{7-\delta}$ compounds was determined by thermogravimetric analysis (TGA) from measurements of the weight change as a function of temperature in both air and in an oxygen atmosphere. An MgO sample holder was used for the yttrium compound and a platinum sample holder was used for the other four samples, since the temperatures of the TGA curves were below those at which any reactions with platinum were observed. The ground powder was heated from 50°C to 850°C at a rate of 2°C per min to measure the change of weight, and thereby oxygen uptake and loss. The maximum observed weight was assumed to correspond to full oxygenation of seven oxygen atoms, or Ba$_2$RCu$_3$O$_7$. The weight loss at a given temperature was then used to compute the oxygen content. The correspondence between oxygen content and quenching temperatures was thus established.

Due to the difficulty of applying a precise correction for the buoyancy effect, oxygen content established in this way may have an estimated relative uncertainty of ±5% ($k=2$).

Digital x-ray data were collected at room temperature on a computer-controlled powder diffractometer equipped with a focusing graphite crystal monochromator and a theta-compensating slit. Copper radiation (CuK$_\alpha$, $\lambda = 1.5405981$ Å [50]) was employed for all studies. Two certified $d$-spacing standards: silicon, SRM640b [51], and fluorophlogopite, SRM675 [52] were used as internal standards for calibration [53]. Sample preparation, mounting methods and data processing followed those described by McMurdie et al. [54].

The flux exclusion of these powders was studied by using a computerized ac magnetometer. A sample powder of 10 mg to 20 mg was packed in a small, non-magnetic holder and mounted on a stage containing a calibrated silicon diode thermometer. The ac susceptibility was measured as a function of temperature from 300 K to 20 K for most samples in a Hartshorn type bridge circuit at a frequency of 1.68 kHz. The magnitude of the applied ac field was about $0.5 \times 10^{-4}$ T. The relative Meissner effect was detected by observing the real part of the signal arising from the diamagnetism of the sample. We define the superconducting onset temperature, $T_{CO}$, as the temperature at which the ac susceptibility deviates from the near zero value of the normal state.

3. Results and Discussion

The x-ray spectra of Ba$_2$RCu$_3$O$_{7-\delta}$ ($\delta$ from 0 to 1) are, in general, similar to the yttrium analogs [24]. The progressive changes of shape and the indexing of peaks in the five main regions of the Bragg angle, $2\theta$, around 32° to 33°, 38° to 39°, 45° to 49°, 57° to 60°, and 68° to 70° reveal the crystallographic phase transition from orthorhombic to tetragonal for all compounds. Figure 2 illustrates the diffraction patterns of the Ba$_2$NdCu$_3$O$_{7-\delta}$ samples quenched from various temperatures at 401°C, 545°C, 570°C, 578°C and 592°C. These diffraction patterns demonstrate a gradual reduction in orthorhombicity as evidenced, for example, by the peak shape changes for the 200 and 020 reflections at 46° to 48° $2\theta$ and the 213 and 123 reflections at 57° to 59° $2\theta$.

3.1 Lattice Parameters

The oxygen content of the Ba$_2$RCu$_3$O$_{7-\delta}$ compounds was determined by thermogravimetric analysis (TGA) from measurements of the weight change as a function of temperature in both air and in an oxygen atmosphere. An MgO sample holder was used for the yttrium compound and a platinum sample holder was used for the other four samples, since the temperatures of the TGA curves were below those at which any reactions with platinum were observed. The ground powder was heated from 50°C to 850°C at a rate of 2°C per min to measure the change of weight, and thereby oxygen uptake and loss. The maximum observed weight was assumed to correspond to full oxygenation of seven oxygen atoms, or Ba$_2$RCu$_3$O$_7$. The weight loss at a given temperature was then used to compute the oxygen content. The correspondence between oxygen content and quenching temperatures was thus established. Due to the difficulty of applying a precise correction for the buoyancy effect, oxygen content established in this way may have an estimated relative uncertainty of ±5% ($k=2$).
The structural transition temperature for the other lanthanide analogues were found to be as follows: Sm: 625 °C to 650 °C, Gd: 650 °C to 660 °C, Y: 708 °C to 720 °C, Ho: 748 °C to 761 °C, and Er: 750 °C to 770 °C [36-39, 41-49]. The tetragonal-orthorhombic structural transition temperatures are summarized in Table 2 along with ionic radii of the lanthanide ions, R$^{3+}$ [56] and the estimated oxygen composition.

Table 3 gives the cell parameters of Ba$_2$NdCu$_3$O$_{7-\delta}$ as a function of quenched temperatures (°C). Number in parenthesis indicates one standard deviation from results of least-square refinements [37].

Table 3. Least-squares cell parameters for Ba$_2$NdCu$_3$O$_{7-\delta}$ as a function of quenched temperatures (°C). Number in parenthesis indicates one standard deviation from results of least-square refinements [37].

| Quenched temperatures | $a$(Å) | $b$(Å) | $c$(Å) | V(Å$^3$) |
|-----------------------|--------|--------|--------|----------|
| 401                   | 3.8681(11) | 3.9180(3) | 11.762(3) | 178.26(7) |
| 464                   | 3.8676(14) | 3.9223(8) | 11.779(2) | 178.69(6) |
| 501                   | 3.8724(7)  | 3.9237(12) | 11.781(2) | 179.00(5) |
| 556                   | 3.882(2)   | 3.9180(12) | 11.792(4) | 179.30(9) |
| 570                   | 3.887(2)   | 3.9115(5)  | 11.797(2) | 179.35(8) |
| 578                   | 3.9034(6)  | 3.9103(14) | 11.8105(14) | 179.98(5) |
| 592                   | 3.9054(4)  | 3.9136(11) | 11.8336(11) | 180.46(3) |
| 697                   | 3.9029(3)  | 3.9056(12) | 11.8511(12) | 180.48(3) |
| 800                   | 3.9000(3)  | 3.9000(3)  | 11.8564(12) | 180.34(3) |

The variation with annealing temperature of the $c$ axis cell dimension and the cell volume of these six compounds is illustrated in Fig. 4. Although these curves show, in general, the expected trend of increasing value as the temperature increases, the Ba$_2$GdCu$_3$O$_{7-\delta}$ compounds behave somewhat differently. For example, the $c$-dimension did not fall in the expected order relative to the other compounds. By analogy with the yttrium system, the elongations along the $c$ axis of these compounds are considered to be due to the increased number of oxygen vacancies. At 400 °C the relative $c$ axis cell dimensions of these compounds are as expected: $c_{\text{Nd}} > c_{\text{Sm}} > c_{\text{Gd}} > c_{\text{Y}} \sim c_{\text{Ho}} > c_{\text{Er}}$. At higher temperature the trend alters and becomes $c_{\text{Nd}} > c_{\text{Sm}} > c_{\text{Gd}} > c_{\text{Y}} > c_{\text{Er}} > c_{\text{Ho}}$. The volume plots in Fig. 5 illustrate the expected trends in volume expansion as the annealing temperatures increase, namely, $V_{\text{Nd}} > V_{\text{Sm}} > V_{\text{Gd}} > V_{\text{Y}} \sim V_{\text{Ho}} > V_{\text{Er}}$.

Figure 6 shows the first derivative of the TGA curves against temperature for the six compounds. While the weight change curves (not shown) are continuous, the first derivatives show relatively abrupt changes in slope. The temperature at which this abrupt change in temperature takes place can be considered as due to a phase transition, presumably the orthorhombic/tetragonal transition, and the trend of this behavior therefore parallels that listed in Table 2, namely, the lanthanide elements with a smaller ionic radius stabilize the orthorhombic phase to higher temperatures.
Fig. 3. Crystallographic dependence of the $a$ and $b$ axes of $\text{Ba}_2\text{RCu}_3\text{O}_{7-\delta}$ on the annealing temperature. Lanthanide ion $R$: (a) Nd (b) Sm (c) Gd (d) Y (e) Ho, and (f) Er.
3.2 Chain-Oxygen Order-Disorder Transition

Figure 7 shows the structure of Ba$_2$RCu$_3$O$_{7–\delta}$ with the labeling of atoms and the oxygen sublattice site. Curve (a) of Fig. 8 shows a plot of these experimental transition temperatures as a function of the ionic radius of the R$^{3+}$ ions. An obvious trend is observed. Lanthanide elements of smaller ionic size stabilize the orthorhombic phase to a higher temperature as well as to lower oxygen content. This trend can be understood in terms of order-disorder theory.
The fraction averaged over both sublattices (c). Oxygen-oxygen pairs, and the fractional site occupancy parameter (p) of near-neighbor pair sites occupied by oxygen-oxygen near neighbor pairs. In Eq. (1), k is the Boltzmann constant. The long-range order parameter is defined such that the fractional site occupancy of oxygen on one of the two sublattice site is \( c = (1+S) \), while that on sublattice \( \alpha \) is \( c = (1-S) \). In \( Ba_2YCu_3O_7-\delta \), \( c \) is assumed to be 0.5 when \( \delta \) is zero, and \( \delta = 1-2c \). The order-disorder transition temperature (orthorhombic to tetragonal), \( T_{o-t} \), is therefore related to the oxygen-oxygen repulsion energy, \( v \), on the two sublattice sites and the value of the average site occupancy \( c \) by

\[
kT_{o-t} = v \ln\{16(1-c)/[1-4(1-2c)^2]\}.
\]

The trend of dependence of the ionic radius across the lanthanide series using the QCA is summarized in Fig. 8. The upper curve (a) represents the experimental data taken from this work while the lower one (b) represents the theoretical results using the current data (i.e., experimental phase transition temperatures) [40].

The theoretical data are calculated by using the transition temperature of \( Ba_2YCu_3O_7 \) as a reference (transformation takes place at an oxygen content of 6.5). The calculated results agree with experimental data in that the larger the ionic size of \( R \), the lower the orthorhombic/tetragonal phase transition temperature. The observable difference in these two curves is partly because the orthorhombic to tetragonal transition in the \( R \)-systems takes place at an oxygen content different from that of the reference \( Y \)-system, namely, 6.4 (Er) to 6.83 of Nd. The formation energy of Frenkel pairs is altered because of the difference of oxygen content which affect lattice parameters and atomic positions. This formation energy of Frenkel pairs decreases as anisotropy in the \( ab \) plane \([b-a]/a\] decreases.

From a simple point of view, if an assumption is made that the orthorhombic phase (absence of oxygen on the \( a \) axis) is favored at lower temperatures, then as the size of the lanthanide ion decreases, so does the distance between neighboring basal oxygens; the repulsion energy, \( v \) (Fig. 7), between these oxygens increases correspondingly. The transformation temperature, according to Eq. (2), is directly proportional to the repulsion energy, and is therefore higher the smaller the size of \( R \).

### 3.3 \( T_c \) Dependence of Oxygen Content

Figure 9 shows a typical plot of the rationalized ac susceptibility of \( Ba_2RCu_3O_{7-\delta} \) [31] as a function of temperature. The annealing temperatures are indicated from 400 °C to 708 °C. A bulk sample exhibiting 100 % flux exclusion would have an ac susceptibility.
of −1 (dimensionless). Finnemore et al. [59] has shown that 100% flux exclusion is not expected for fine powders of a completely superconducting material. It is thus not possible to determine exactly the fraction of the sample that is superconducting from the curves of Fig. 9. However, these curves have the approximate shape and magnitude expected for a ratio of particle diameter to superconducting penetration depth between 2 and 10 [59]. The decrease in the magnitude of the flux exclusion seen in Fig. 9 for the samples annealed at higher temperatures can be due either to a decrease in the fraction of the materials that is superconducting or to an increase in the superconducting penetration depth, or likely, to a combination of both.

Figure 10 shows plots of the superconducting transition temperature, as determined by ac magnetic susceptibility, on the annealing temperature in Ba$_2$RCu$_3$O$_{7-δ}$ with R = Nd, Sm, Gd, Y, Ho, and Er.

Fig. 9. A plot of the rationalized ac susceptibility as a function of temperature. The annealing temperatures are indicated. All samples were fully packed fine powders. Samples annealed at 750 °C and above did not exhibit any flux exclusion.

Fig. 10. Dependence of the superconducting transition temperature, as determined by ac magnetic susceptibility, on the annealing temperature in Ba$_2$RCu$_3$O$_{7-δ}$ with R = Nd, Sm, Gd, Y, Ho, and Er.
urements as a function of the annealing temperature for all six compounds. Two apparent plateaus in $T_{CO}$ were observed for the materials with yttrium, holmium and erbium substitution: one at 83 K to 92 K and the other at 58 K to 60 K. Narrower and somewhat lower plateaus were detected for the gadolinium, samarium and neodymium compounds. Although, in general, the orthorhombic structure is superconducting whereas the tetragonal is not, this structure correlation does not appear to be exact. For example, the tetragonal yttrium material annealed at 719 °C is superconducting, whereas the orthorhombic Er compound annealed at 750 °C is a non-superconductor. Furthermore, despite reports from literature that even in the Ba$_2$YC$_3$O$_7$ system alone, one can achieve plateau features varying from broad plateaus at 60 K and 90 K to complete absence of plateaus depending on how samples were prepared [60], our samples were all prepared under similar conditions, therefore it is possible that one should be able to correlate the features of these plateaus with size of $R$.

Figure 11 depicts the oxygen content dependence of the transition temperatures of these six compounds as derived from thermogravitmetric analysis/differential thermal analysis (TGA/DTA) data. It is noteworthy that a correlation exists between the size of the $R^{3+}$ ion and both the phase transition temperatures (or oxygen compositions) and $T_c$ values for these plateaus, as is summarized in Table 4. Compounds with a smaller size lanthanide $3^{+}$ ion have a tendency to have both a wider 90 K plateau in $T_c$ and a wider and relatively higher $T_c$. 

![Fig. 11. Dependence of superconducting transition temperature, as determined by ac magnetic susceptibility, on the oxygen content in Ba$_2$RC$_3$O$_7$-$\delta$, with $R =$ Nd, Sm, Gd, Y, Ho and Er.](image)

**Table 4.** Characteristics of the low temperature $T_c$ plateaus for Ba$_2$RC$_3$O$_7$-$\delta$ with $R =$ Nd, Sm, Gd, Y, Ho, and Er

| Lanthanide | Approximate compositional range $(x = 7-\delta)$ | Approximate anneal temperature range in air | $T_c$ |
|-----------|-----------------------------------------------|--------------------------------------------|-------|
| Nd        | $6.83 < x < 6.88$                             | $40 ^\circ C$ (460 $^\circ C$ to 500 $^\circ C$) | 55 K  |
| Sm        | $6.82 < x < 6.83$                             | $70 ^\circ C$ (550 $^\circ C$ to 620 $^\circ C$) | 52 K  |
| Gd        | $6.77 < x < 6.81$                             | $70 ^\circ C$ (580 $^\circ C$ to 650 $^\circ C$) | 38 K  |
| Y         | $6.62 < x < 6.80$                             | $100 ^\circ C$ (600 $^\circ C$ to 700 $^\circ C$) | 58 K  |
| Ho        | $6.62 < x < 6.77$                             | $80 ^\circ C$ (580 $^\circ C$ to 660 $^\circ C$) | 60 K  |
| Er        | $6.58 < x < 6.80$                             | $120 ^\circ C$ (600 $^\circ C$ to 720 $^\circ C$) | 60 K  |
in the 50 K to 60 K range. The Nd, Sm and Gd samples behave otherwise. They lack any obvious 90 K plateau, and they also play a narrow low \( T_c \) plateau (55 K, 52 K and 38 K, respectively). The observed trends appear to differentiate the early and later members of the lanthanide series.

### 3.4 Structural Features of \( \text{Ba}_2\text{RCu}_3\text{O}_{7−\delta} \)

The behavior of the curves of \( T_c \) versus annealing temperature (Fig. 10) and \( T_c \) versus oxygen content (Fig. 11) suggests the presence of more than one structural phase. X-ray results indicated both to be orthorhombic and they are designated here as O(A) and O(B). Other studies such as that of Cava et al. [41] have suggested that the second plateau region indicates the presence of a second orthorhombic phase. The presence of an O(B) phase in the yttrium sample has been confirmed by electron diffraction studies, which gave information about the degree to which ordering of the oxygen ions had occurred in the specimens. Diffraction patterns from the yttrium specimens (Y6.85, Y6.63, and Y6.55, as defined in Table 1) contained elongated superlattice reflections (streaks) lying along the [100] direction and centered on positions \( g + ½00 \) in reciprocal space (where \( g \) is a reciprocal lattice vector of the conventional orthorhombic structure).

A typical image of a crystallite in the yttrium specimen, Y6.55, together with a diffraction pattern from the crystallite, are shown in Fig. 12. The image, Fig. 12(a), shows an approximately regular arrangement of twins. From the diffraction pattern, Fig. 12(b), we can determine that the habit plane of the twins is (110), as expected, and that the orthorhombicity (\( b/a \)) of the material is 1.01, which agrees with the value of 1.008 obtained previously [37]. Diffuse scattering spots were also observed in the diffraction patterns, as indicated by the arrows. Despite the twinning, by a careful examination of the diffraction pattern far from the transmitted beam where the splitting of the orthorhombic matrix spots was greatest, it was possible to determine that the superlattice streaks were at \( g + ½00 \) and not \( g + 0½0 \). This corresponds to a doubling of the unit cell dimension along the \( a \) axis, suggesting that the oxygen atoms of every other CuO chain, running along the \( b \) axis, are removed. These results agree with those reported by Alario-Franco et al. [42], who observed diffuse scattering in a \( \text{Ba}_2\text{YCu}_3\text{O}_{7−\delta} \) \( \delta = 0.5 \) sample. For the yttrium specimen, Y6.85, the streaks at \( ½00 \) were particularly faint and long, as is expected as the oxygen content increases. In all cases where superlattice streaks were observed, there was variation in both the intensity and length of the streaks between different grains from the same specimen, indicating that the oxygen content was not constant throughout the specimen and that the diffusion of oxygen through the lattice is slow at these temperatures. However, on average, the lengths of the streaks for specimens Y6.63 and Y6.55 corresponded to short range order on the 5 nm to 10 nm (50 Å to 100 Å) scale.

Although short range ordering was observed in the Y sample using electron diffraction, long range ordering was not observed using either electron diffraction or powder x-ray diffraction. Neutron scattering studies on a 60 K yttrium material annealed at 640 °C also showed no evidence of long range ordering. The results agreed with those of the x-ray powder diffraction and indicate the absence of any doubling of the cell parameters along either the \( a \) or \( b \) axis. The nature of supercell ordering in Y-123 \( \text{Ba}_2\text{YCu}_3\text{O}_{7−\delta} \) have been studied extensively by Beyers et al [61], Zeise et al. [62], and Ourmazd and Spence [63]. De Fontaine et al. [64] suggested that this supercell is stabilized at low temperature. It is now generally agreed that the degree of plateau behavior of \( \text{Ba}_2\text{YCu}_3\text{O}_{7−\delta} \) depends on the degree to which the ordered 2\( a \times b \times c \) supercell is stabilized [65].

The gadolinium specimen was unique in that there was very little twinning in the crystallites studied; all the other lanthanide specimens were twinned. Diffraction patterns from the neodymium, samarium and gadolinium specimens (Nd6.90, Sm6.75 and Gd6.79) showed no evidence of superlattice formation of the type corresponding to the doubling of the unit cell dimension along the \( a \) axis. It is conceivable that the O(B) phase in compounds with smaller size \( R \), has a doubling of the unit cell dimension along the \( a \) axis, corresponding to the absence of oxygen in every other Cu-O chain along the \( b \) axis. For the larger size \( R \), the compositions with lower \( T_c \) plateau that we investigated correspond to those deviating significantly from the oxygen content of 6.50. We postulate that these lower \( T_c \) plateau regions of 55 K, 52 K, and 38 K in the Nd, Sm and Gd samples may result from another orthorhombic phase with a superlattice cell of the type corresponding to different oxygen vacancies. A superlattice cell other than the type with \( \delta = 2a \) has also been reported. For example, Alario-Franco et al. [42] reported a superlattice type in the Y compound corresponding to an oxygen content of 6.85; this superlattice can be indexed on a unit cell of \( 2\sqrt{2}a_1 \times 2\sqrt{2}a_2 \times 3a_3 \), where \( a_1 \) is the basic cubic perovskite cell dimension.
Fig. 12(a). TEM micrograph of Ba$_2$YCu$_3$O$_{7-\delta}$ grain annealed at 675 °C for 21 h showing typical twin boundary arrangement.

Fig. 12(b). Electron diffraction pattern from the grain shown in Fig. 12(a). The diffuse spots (indicated by arrows) correspond to a doubling of the $a$ axis (a superlattice index-able with a cell of $a' = 2a$). Twinning is demonstrated by the splitting of the diffraction spots.
Oxygen stoichiometry is an important parameter affecting the $T_c$ depression and the presence of $T_c$ plateaus. The CuO chain in the basal plane and the CuO plane \cite{66-69} can be considered as an interacting electronic unit. Tokura et al. \cite{70} and Cava et al. \cite{41,71} have suggested that the chains function as a charge reservoir which controls the electron density on the Cu-O planes. By applying this concept to our samples, when oxygen atoms are removed from the chains, the electrons which were bound to them are transferred to the lowest unoccupied energy level. When the total oxygen content is near 7, the $T_c$ value of 90 K is due to the coupling of the chains and the planes. As illustrated in Fig. 13, when oxygen atoms are removed from the chains, the chain copper-bridging oxygen distance, Cu(1)-O(1), becomes shorter and the plane copper-bridging oxygen distance, Cu(2)-O(1), becomes longer, with the result that the chains and the planes become decoupled. The distance Cu(1)-O(1) first shortens gradually in the orthorhombic O(A) region, then changes rather sharply in region B \cite{36,72}. In the tetragonal region it resumes a much smaller slope. The Cu(2)-O(1) bond elongates in a similar way in these materials. It appears that the decoupling effect of the chains and the planes takes place much more dramatically in region O(B). The observed superconductivity at the lower $T_c$ regions of 60 K, 60 K, 58 K, 38 K, 52 K and 55 K in the Er, Ho, Y, Gd, Sm and Gd compounds, respectively, is probably due to sufficient decoupling of the chain-plane unit, and the different $T_c$ are intrinsic.

**Fig. 13.** Illustration of the bond lengths, Cu(1)-O(1) and Cu(2)-O(1), as a function of oxygen content in the Ba$_2$YCu$_3$O$_{7-\delta}$ samples.
values of the plane. When the capacity of the CuO chain-reservoirs to hold charge is exhausted, charge is transferred from the chains to planes, and superconductivity disappears. This charge transfer is equivalent to a decrease in the hole concentration in the planes [41,70].

4. Conclusions

The structural phase transformation that occurs in the high-$T_c$ ceramic superconductors is of considerable importance in the processing of these materials. We have found that the temperature of this structural phase transition, its oxygen stoichiometry, and characteristics of the associated $T_c$ plateaus follow a trend depending on the ionic radius of the lanthanide ions. Lanthanide elements with a smaller ionic size stabilize the orthorhombic phase to higher temperatures, or lower oxygen content. The superconducting temperature is less sensitive to the oxygen content for materials with smaller ionic radii.

Electron microscopy studies indicated that the O(B) phase in the Y compound has a doubling of the unit cell dimension along the $a$ axis, corresponding to the absence of oxygen in every other Cu-O chain along the $b$ axis. While not yet investigated, this type of superlattice can probably also be found in Ba$_2$RCu$_3$O$_{7-\delta}$ compounds with smaller size R. This is most likely short-range ordering as both the x-ray and neutron diffraction data indicate a lack of evidence for a long-range ordering of oxygen in samples quenched around the “lower” $T_c$ plateau region. For the lanthanide samples with larger size of R (i.e., Nd, Sm, and Gd), the lower $T_c$ plateau is postulated as corresponding to a different superlattice resulting from different oxygen stoichiometry.

Our study also illustrates the importance of strain effects on the orthorhombic/tetragonal phase transition in the Ba$_2$RCu$_3$O$_{7-\delta}$ compounds. The formation energy of Frenkel pair defects as a function of volumetric strain for Ba$_2$RCu$_3$O$_{7-\delta}$ and for Ba$_2$YCu$_3$O$_7$ under hydrostatic pressure show good agreement with experimental observations that pressure favors ordering of the CuO chains. For example, the Frenkel pair formation energy indeed increases significantly (around $-0.25$ eV/0.01 volumetric strain) under compression. Based on a quasi-chemical approach, the orthorhombic/tetragonal transition temperatures for Ba$_2$RCu$_3$O$_{7-\delta}$ have been computed by scaling the effective oxygen-oxygen short-range repulsive energy in the CuO chain using the Frenkel pair formation energy. The calculated results agree with experimental data in that the larger the ionic size of the lanthanide, the lower the orthorhombic/tetragonal phase transition temperature.

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