Assessing the Mechanisms Thought to Govern Ice and Snow Friction and Their Interplay With Substrate Brittle Behavior

James H. Lever*, Emily Asenath-Smith, Susan Taylor and Austin P. Lines

Cold Regions Research and Engineering Laboratory, US Army Engineer Research and Development Center, Hanover, NH, United States

Sliding friction on ice and snow is characteristically low at temperatures common on Earth’s surface. This slipperiness underlies efficient sleds, winter sports, and the need for specialized tires. Friction can also play a micro-mechanical role affecting ice compressive and crushing strengths. Researchers have proposed several mechanisms thought to govern ice and snow friction, but directly validating the underlying mechanics has been difficult. This may be changing, as instruments capable of micro-scale measurements and imaging are now being brought to bear on friction studies. Nevertheless, given the broad regimes of practical interest (interaction length, temperature, speed, pressure, slider properties, etc.), it may be unrealistic to expect that a single mechanism accounts for why ice and snow are slippery. Because bulk ice, and the ice grains that constitute snow, are solids near their melting point at terrestrial temperatures, most research has focused on whether a lubricating water film forms at the interface with a slider. However, ice is extremely brittle, and dry-contact abrasion and wear at the front of sliders could prevent or delay a transition to lubricated contact. Also, water is a poor lubricant, and lubricating films thick enough to separate surface asperities may not form for many systems of interest. This article aims to assess our knowledge of the mechanics underlying ice and snow friction. We begin with a brief summary of the mechanical behavior of ice and snow substrates, behavior which perhaps has not received sufficient attention in friction studies. We then assess the strengths and weaknesses of five ice- and snow-friction hypotheses: pressure-melting, self-lubrication, quasi-liquid layers, abrasion, and ice-rich slurries. We discuss their assumptions and review evidence to determine whether they are consistent with the postulated mechanics. Lastly, we identify key issues that warrant additional research to resolve the specific mechanics and the transitions between them that control ice and snow friction across regimes of practical interest.

Keywords: tribology, wear, pressure-melting, self-lubrication, quasi-liquid layers, abrasion, ice-rich slurries
INTRODUCTION

Sliding friction on ice and snow is remarkably low at temperatures common on Earth’s surface. This slipperiness underlies efficient sleds for polar transport, competitive and recreational winter sports, and specialized vehicle tires (e.g., De Koing et al., 1992; Higgins et al., 2008; Scherge et al., 2013; Nachbauer et al., 2016a; Lever et al., 2016). Friction can also play a micro-mechanical role affecting ice compressive and crushing strengths (e.g., Schulson, 2001). Researchers have proposed several plausible mechanisms that focus on the properties of ice near its melting point. Kietzig et al. (2010) and Colbeck (1992) provided comprehensive reviews of these hypothesized mechanisms for ice and snow substrates, respectively. However, directly validating these mechanisms has been difficult owing to the small length scales and time intervals of surface interactions. Nevertheless, recent advances in imaging and surface-measurement technology have provided new insight and the potential to discern between hypothesized mechanisms governing friction on ice and snow. This article aims to assess our knowledge of the mechanics underlying ice and snow friction. Our focus is on kinetic friction relevant to dynamic systems rather than slower motion relevant to glaciers or stationary structures. Owing to competitive or safety interests, much research has aimed to understand friction governing sports equipment (e.g., skis, skates, sled-runners) and vehicles (e.g., tires, cargo sleds), largely relying on the tenets of self-lubrication theory. This approach is slowly changing as more observational evidence emerges on the roles of other mechanisms.

We begin with a review of the mechanical properties of ice and snow (Ice and Snow Mechanical Behavior) and discuss how those properties influence friction mechanics. We then summarize five ice- and snow-friction hypotheses and assess their strengths and weaknesses:

- Pressure melting—the reduction in phase-transition temperature by slider pressure
- Self-lubrication by a melt-water film produced by frictional heating
- Quasi-liquid surface layers on ice that display increased molecular mobility compared with the bulk crystal structure
- Abrasion of ice or snow-grains by slider asperities and the role of the resulting wear particles as dry lubricants
- Ice-rich slurries formed by crushing or abrasion that act as lubricating layers with viscoelastic rheology

In Evidence of Ice- and Snow-Friction Mechanisms, we summarize observations that support or challenge these hypotheses. Lastly, we identify key issues that warrant additional research to resolve the specific mechanics and the transitions between them that control ice and snow friction across regimes of practical interest.

ICE AND SNOW MECHANICAL BEHAVIOR

Ice and bulk snow show complex mechanical behavior that can vary with temperature, load rate, microstructure and morphology (Petrovic, 2003). We focus here on relatively rapid loading that induces elastic deformation and brittle failure within the ice or snow, a regime that governs most kinetic-friction scenarios. For example, interactions between micron-scale asperities would occur on ms time scales for 1 mm s⁻¹ sliding speeds. Rapid macro-scale indentation of bulk ice or natural snow also causes brittle fracture of the substrate. The cited studies also provide guidance on substrate behavior at lower interaction rates, should those conditions be relevant to the sliding-system of interest.

Ice Under Compression and Tension

Solid ice is remarkably brittle right up to its melting point (Schulson, 2001). Under uniaxial compression, brittle failure occurs at strain rates above 10⁻⁴–10⁻³ s⁻¹ and at strengths of about 10 MPa at −10°C (Hawkes and Mellor, 1972; Gold, 1977; Schulson, 2001). Strain at failure is on the order of 10⁻³. The strain rate for transition from ductile to brittle failure decreases, and compressive strength increases, with decreasing temperature (Arakawa and Maeno, 1997; Schulson, 2001). Young’s modulus for rapidly loaded ice ranges 6–10 GPa, increasing with loading rate, and Poisson’s ratio ranges about 0.28–0.36 (Gold, 1977; Gold, 1988).

For ice specimens well bonded to the platens, compressive failure usually occurs through shear faulting. In this mode, wing cracks form at the tips of sliding cracks and open in tension, at rates controlled by the sliding friction of opposing faces of the main cracks. The material strain-softens but continues to carry load. Friction coefficients of these sliding cracks range μ ~ 0.3–0.8, increasing with decreasing temperature (Schulson, 2001). Interestingly, Schulson (1990) noted that this sliding can produce powderized ice on the fractured surfaces from localized failures. Confinement increases failure stresses, and the ice becomes more ductile at high confining pressures; the reduction in melting point limits the increase in deviatoric stress at failure (Schulson, 2001).

In tension, brittle fracture dominates ice failure at strain rates higher than about 10⁻³ s⁻¹. Uniaxial tensile strength is about 1–2 MPa for granular ice under brittle failure and is nearly independent of temperature from −40 to 0°C. (Hawkes and Mellor, 1972; Gold, 1977; Schulson, 2001). Strain at failure is on the order of 10⁻³. Fracture processes (crack initiation and propagation) govern brittle tensile strength. Even as warm as −2°C, freshwater ice at high loading rates is more brittle than rocks and ceramics, with fracture energy ~0.5 Jm⁻² or just 2.5 times higher than the surface energy required to create two new surfaces (Nixon and Schulson, 1987). This extreme brittleness also influences the response of ice to rapid indentation and shear.

Ice Indentation

Hardness, or average indentation pressure, is often considered a material property, and hardness under spherical indentation relates to tensile yield stress for ductile materials (Bowden and Tabor, 1954; Bhushan, 2013). However, brittle failure can introduce important variations in indentation resistance with indenter geometry and rate. Considerable research effort has sought to understand the mechanics of ice indentation to aid...
The vast majority of the applied load is compressive. Indentation contact zone as friction on skate blades, sled runners or, potentially, surface to ice loads. Here, we review some of this research relevant to ice. Gagnon (1994a; Wells et al., 2011; Kim et al., 2012; Browne et al., 2013) used high-speed video (30,000 frames s⁻¹) to capture the flow of ice-water jets exiting HPZs. These crushing and slurry-creation and -extrusion processes could play important roles at local slider-ice contacts, either from overall slider geometry or from surface asperities.

### Snow Under Compression and Tension

Snow is a porous aggregate of fairly weakly bonded grains of ice. Its strength varies with density, sintering time and loading rate (Mellor, 1964; Mellor, 1975; Abele and Gow, 1975; Salm, 1982; Shapiro et al., 1997; Marshall and Johnson, 2009). Compressive, tensile and shear strengths under rapid loading (brittle failure, strain rates greater than ~10⁴ s⁻¹) range 10 kPa–1 MPa, generally increasing with density across a range 100–600 kg m⁻³. Failure strain is on the order of 10⁻³. Young’s modulus increases from roughly 0.1 MPa to 1 GPa across this density range, whereas Poisson’s ratio ranges about 0.23–0.30, showing a slight increase with density (Mellor, 1964; Mellor, 1975). The specific fracture energy of snow can range 0.1–1 J m⁻² (Reuter et al., 2019). Temperature has less influence on snow strength, especially under brittle failure. Although snow mechanical properties vary strongly with density, variations at a given density are significant and reflect the development of intergranular bonds as the constituent ice grains sinter together. This is especially noticeable for mechanically worked snow used to create roads and runways (Fukue, 1979; Abele, 1990). Snow can also lose strength over time as metamorphism produces layers of large, weakly bonded grains (Schweizer et al., 2003; Blackford 2007; Reuter et al., 2019).

### Combined Compression and Shearing of Snow

Researchers have long recognized that sliders (e.g., skis or sleds) perform work to compact snow to support slider weight (Nakaya et al., 1936; Bekker, 1956; Wong, 1989; Colbeck, 1992). This compaction begins as dry contact at the front of a slider and is rapid enough to cause brittle failure of the snow through rupture of intergranular bonds. Even well-sintered snow can fail in this manner. The concurrent response of the snow to slider shear has not received much attention, yet the resulting snow-grain motion can produce low slider friction. Nakaya et al. (1936) used thin planes of soot and red ochre to track the displacement of natural snow beneath the tracks of skis and sleds for common alpine skiing speeds and normal loads. They found that the slider often displaced the snow at the slider-contact surface several meters longitudinally (down-track), and the sub-track displacements formed a parabolic shape suggestive of fluid-like shear of the powdery snow, despite its compaction by the slider (Figure 2).
Kuroiwa (1977) observed similar down-track shearing profiles of snow compacted under a ski. Mellor (1975) suggested that shearing of fluidized snow imparts friction on the solid boundary similar to turbulent flow.

Rapid compression can also produce pore-pressure lift on a ski or snowboard by pumping air through the dynamically compressed porous snow (Feng and Weinbaum, 2000; Wu et al., 2005; Wu et al., 2006). For moderate snow density (400 kg m$^{-3}$) and slider speed >10 m s$^{-1}$, predicted pore-pressure lift can exceed the vertical support of the solid matrix and thereby reduce contact forces on the snow grains and thus contact friction. The resulting "aerodynamic" drag then becomes important. While Wu and Sun (2011) examined the role of snow-slider friction on pore-pressure lift, the interplay between this lift mechanism and the mechanics of contact friction has not been explored. Additionally, the porous-flow theory as formulated omits longitudinal movement of the fractured grains in response to slider shear.

It seems unlikely that sintering can reform intergranular bonds to arrest snow-grain motion under a slider, although some evidence exists that sintering can proceed quickly. Gubler (1982) measured the development of tensile strength of two ice cones after contact times of 1–500 s. Federolf et al. (2004) observed densified bulbs of snow fragments at the front of an indenter under rapid penetration (up to 2 m s$^{-1}$) and suggested that the fragments sintered quickly. Szabo and Schneebeli (2007) demonstrated sub-second sintering of two ice specimens during brief contact. However, none of these tests imposed concurrent shear motion. If snow-grain translation or rotational motion prevents intergranular bonds from reforming, the snow fragments essentially form a cohesionless granular material.

Lever et al. (2018), Lever et al. (2019) noted that snow friction can be quite low under these conditions.

**Summary of Ice and Snow Mechanical Behavior**

The mechanical behavior of ice and snow can strongly influence contact mechanics on these substrates. Micro-scale asperity interactions, and most macro-scale slider interactions, occur at strain rates sufficient to produce brittle substrate behavior. Ice is extremely brittle right up to its melting temperature. Ice hardness varies with indenter geometry and speed, and brittle crushing can produce ice-rich slurries at the interface that govern contact processes. Slider normal and shear loads can cause snow intergranular bonds to fail, which can prevent warming and melting of persistent contacts. Snow-grain sintering is unlikely to reform these bonds until after the slider has passed. The brittle behavior of ice and snow warrants thorough consideration for its role in influencing friction on these substrates.

**POSTULATED ICE AND SNOW FRICTION MECHANISMS**

**Pressure Melting**

On Earth’s surface, water is denser than ice (hexagonal-structure ice Ih). Consequently, increased hydrostatic pressure aids the phase change from ice to water. Pressure depresses the melting temperature of ice from the ice Ih-liquid-vapor triple point (0.01°C, 611.7 Pa) to the ice Ih-ice III-liquid triple point at −21.985°C and 208.6 MPa (Wagner et al., 2011; Figure 3). The effect is weak: pressure depresses the melting point by only...
−0.074°C MPa⁻¹ near 0°C. The system must also provide the change in enthalpy (latent heat) needed to melt ice, \(dH\):

\[
dH = dE + PdV
\]  

(2)

Work done through the volume change, \(PdV\), reduces the required change in internal energy, \(dE\), by less than 10% (Bridgman, 1912); heat transfer from the surroundings must provide the remainder.

Reynolds (1899) postulated that a thin water film formed by pressure melting could account for the slipperiness of ice during skating or walking. Most subsequent researchers dismissed this mechanism owing to the high contact-pressures needed and the requirement of a heat source (Bowden and Hughes, 1939; Colbeck, 1995; Kietzig et al., 2010). Frictional heating from slider motion seemed a direct way to create a lubricating film and did not require high pressures (see Self-Lubrication).

Niven (1959) argued that both pressure and heating could produce water films at contacting ice asperities, citing steel-on-ice tests that showed the friction force approaching a constant value with increasing normal load. However, Niven envisioned plastic deformation during asperity interactions and did not consider that the ice asperity could fracture and fail during such short interactions.

Colbeck (1995) specifically dismissed pressure melting as an important process during ice skating. He argued that pressures needed significantly to reduce the melting point exceeded the crushing strength of ice. While Colbeck noted that failure pressures depended on the state of confinement, he stated that "Indentation hardness experiments [Barnes et al. (1971)] also show that pressure melting is not one of the failure mechanisms when ice is rapidly loaded . . ." However, drop-ball experiments by Kheisin and Cherepano (1973) and Kurdyumov and Kheisin (1979), and indentation tests by Gagnon and Molgaard (1991), showed that pressure melting could play a role by lowering the temperature at which ice melts via energy supplied by the indenter. Ice-rich viscous slurries could consequently form under the indenter.

Colbeck (1995) made two other arguments refuting pressure melting during ice skating: 1) that heat conduction from the ambient to the interface is required and is weak compared with frictional heat generated at the interface, and 2) that any liquid-water films would be squeezed to small thicknesses by the high pressures required for pressure melting. Both arguments warrant reconsideration if the fluid at the interface consists of an ice-rich slurry. This appears to be the case for some ice-friction scenarios.

Certainly, snow is far too weak to support high contact pressures. However, ice is much stronger, and ice-indentation research has revealed that HPZs can reach the pressure-melting point. Furthermore, the slider/indenter can provide the energy needed to melt some fraction of the ice through crushing, shearing and extrusion processes. Localized HPZs could also arise at slider-ice contacting asperities. That is, frictional heat generated by the viscous flow of ice-rich slurries could operate together with pressure-driven lowering of the melting point to provide an efficient lubrication layer between a slider and ice (see Ice-Rich Slurries).

Self-Lubrication

Background

We define the self-lubrication hypothesis as one that attributes the slipperiness of ice and snow to a lubricating melt-water film generated by heat from viscous shearing of that film (Figure 4). This hypothesis allows one to calculate the friction coefficient and heat flux by assuming low Reynolds number (Couette) flow in the sliding direction:

\[
\tau = \eta \frac{dv}{dz} = \eta \frac{v}{h}
\]  

(3)

\[
\mu = \frac{\tau}{\sigma} = \frac{\eta v}{h \sigma}
\]  

(4)

\[
q_f = \tau v = \eta \frac{v^2}{h}
\]  

(5)
where $\tau$ is the shear stress, $\eta$ is the viscosity of water (usually at 0°C), $v$ is slider speed, $h$ is water-film thickness, $\sigma$ is normal pressure, and $q_f$ is frictional heat flux ($Wm^{-2}$).

In its fullest form, the mechanics split $q_f$ into the slider, $q_{fs}$, and into the ice, $q_i$, by equating the contact temperature on each surface to the melting temperature (usually 0°C). Any excess heat melts the contacting ice. The unknown $h$ derives from a mass balance between melt-water production and water-loss from squeezing or shearing of the film by slider normal pressure or forward motion. Because the ice or snow substrate experiences frictional heat for a short duration, $t = l/v$, where $l$ is slider length, most formulations compute the substrate temperature rise using the 1D transient heat-conduction equation (e.g., Carslaw and Jaeger 1959):

$$\Delta T_i = \frac{2q_i}{k_i \pi} \left( \frac{K_i l}{\pi} \right)^{1/2} \tag{6}$$

where $\Delta T_i$ is ice temperature rise, $k_i$ and $K_i$ are ice thermal conductivity and diffusivity, respectively, and $q_i$ is the portion of frictional heat flux that flows into the ice, assumed constant. Eq. 6 can also apply to bulk snow by changing the thermal properties. A transient or a steady-state conduction equation can be used for the slider, depending on the duration of sliding.

Self-lubrication can quantitatively connect $\mu$ to ambient temperature and slider speed, normal pressure and thermal properties. However, it generally does not account for slider surface properties or substrate (ice, snow) mechanical properties. Determining the real area of contact also poses problems, especially at ice asperities and for sliding on snow where contact area evolves. Importantly, it assumes that a self-generated water film forms during sliding without describing how dry contact at the front of a slider or at the start of motion transitions to lubricated contact. Direct asperity contact must occur until the film thickens sufficiently to separate the surfaces.

Bhushan (2013) delineated lubrication regimes based on the ratio of film thickness to roughness:

$$\frac{h}{R_c} < 1 \quad \text{boundary} \quad (7a)$$

$$1 < \frac{h}{R_c} < 5 \quad \text{mixed-mode} \quad (7b)$$

$$\frac{h}{R_c} > 6 \quad \text{hydrodynamic} \quad (7c)$$

where $R_c$ is the composite standard deviation of roughness heights. Friction and wear rates can be high under boundary lubrication, and appreciable solid-solid interactions occur, mediated by molecular-scale films (Jones, 1982; Bhushan, 2013). Within the mixed-mode regime, some solid-solid contacts occur, producing contact friction and wear particles, along with partial hydrodynamic lubrication. For full hydrodynamic lubrication to prevail, the surfaces must be smooth relative to the film thickness to avoid solid-solid contact and for roughness to have negligible effect on squeeze flow (Moore, 1965; Bhushan, 2013). Most self-lubrication formulations fail this test.

Despite these potential drawbacks, self-lubrication remains widely accepted as an explanation for why ice and snow are slippery. Here, we review its development as a friction hypothesis and identify some of its shortcomings.

Self-Lubrication on Ice

Bowden and Hughes (1939) conducted the first systematic tribometer experiments of sliders on solid ice and compacted-snow and suggested that a lubricating film of melt-water from frictional heat could account for low friction on both substrates. They noted that high static friction argued against pressure melting, whereas system changes that increased interface temperatures (e.g., higher ambient temperatures, heat conducted to or trapped at the interface) reduced friction, consistent with their hypothesis. Furthermore, they suggested that the higher friction on snow compared to ice was “...almost certainly due to the extra mechanical work of displacing and compacting the snow” and noted that outdoor tests on actual skis produced lower friction after several repeated passes over the same tracks. While not stated, these snow-friction observations are consistent with intergranular-bond failure and grain movement that would impede persistent heating and melting of individual snow-slider contacts. Later, Bowden (1953) conducted static-friction tests of skis on compacted snow and compared the results with kinetic friction measured using coupons of the same surface treatments contacting a rotating ice disk at 5 m s$^{-1}$. Bowden interpreted the large drop in kinetic vs. static friction as evidence supporting self-lubrication theory. Indeed, post-test freezing of an aluminum coupon to the ice confirmed some friction-induced melting, although Bowden did not report the duration of sliding for these tests.

Evans et al. (1976) accepted the self-lubrication hypothesis and used it to explain the dependence of ice friction on ambient
For theory, they formulated an equation for the heat sinks to balance water production and loss with applied normal load. Their model predicted that it serves to lubricate the surfaces.

However, Evans et al. (1976) also presented evidence that other mechanisms could be important:

- Friction values were lower during the first few revolutions of the ice cylinder, then rose to steady-state values. Lower initial values likely resulted from dry-contact shearing or pressure-melting at ice asperities.
- They noted that “At lower temperatures [≤−2°C] wear was rapid at first, as the pressure exceeded the hardness of the ice, but after a few hundred traversals of the surface it quickly decreased.” This observation is also consistent with dry-contact abrasion or pressure-melting at ice asperities.
- “After a run the rods showed definite signs of abrasion at the areas of contact.” “Abrasion was visible on rods of all the different materials…”
- They noted that if viscous shearing accounted for their measured friction values, h would only be 5 nm or “…much smaller than the surface roughness, and therefore viscous shearing of the water film cannot be the mechanism that produces the friction.”
- “It is clear that mixed lubrication exists: the lubricant supports much of the load between the two surfaces, but at high points the surfaces come into contact or are separated by a film of only a few molecules thick, and these are the sources of most of the frictional force.”

In effect, Evans et al. (1976) analyzed the heat flows from the slider-ice interface without identifying the mechanism that generated the frictional heat. They noted evidence of abrasion and direct slider-ice contact. Nevertheless, they concluded that “…in the range of our experiments, the main contribution to the observed friction comes from a large lubricated area at the melting point rather than a small dry area in front.”

Oksanen and Keinonen (1982) extended self-lubrication theory by assuming that viscous shear of the water film generated the frictional heat. They modeled transient heat flows into both slider and ice, although they independently set the interface melting temperature, $T_m$, and ice hardness, $H_i$ (to establish contact area). Notably, they did not include squeeze flow to balance water production and loss with applied normal load. Their model predicted $\mu \propto v^{-1/2}$ and $\mu \propto v^{1/2}$ at low temperatures and high temperatures, respectively, and model predictions agreed well with their ice-on-ice friction measurements and with those of Evans et al. (1976), with the caveat that they selected rather than calculated $T_m$ and $H_i$.

The Oksanen and Keinonen (1982) model raises several concerns:

- It predicted $h \sim 0.4–6$ nm at −15°C and 40–90 nm at −1°C, yet they did not note that solid-solid contact was likely for such thin films.
- The model did not include water loss from squeeze flow and its consequent reduction of $h$.
- Although the authors extended the model to include a slider steady-state conduction term, that term introduced another independent variable, the thermal-disturbance thickness, to be selected.
- The model did not rigorously predict the interface temperature but rather assumed independent temperature differentials for heat flows into the two bodies.

Stiftler (1984) formulated a first-principles, self-lubrication model by coupling the Reynolds’ equation for hydrodynamic lubrication with an energy equation wherein the source was viscous shearing of a water film and the sinks were transient heat flow into the two bodies and latent heat needed to melt one surface. He recognized that, even for parallel surfaces, steady melting would compensate for mass-loss by squeeze flow to provide normal pressure to support the slider. The model matched surface temperatures to determine the heat flow into each surface and offered two end cases: all the frictional heat flowed into the non-melting surface, or all the heat flowed into the melting surface. The former gave $\mu \propto v^{-1/2}$ while the latter $\mu \propto v^{1/2}$. Applied to an ice skate (−2°C, 1 MPa normal pressure, 1 m s$^{-1}$ speed), Stiftler predicted $\mu = 0.011$ and film thickness $h = 0.17$ μm. Because the formulation required that $h$ be larger than the combined peak roughness of the surfaces, he concluded that “A skater on typical ice would probably fail the test.” Nevertheless, the model formally included all the components of self-lubrication theory.

Makkonen and Tikanmäki (2014) formulated a self-lubrication model that considered $n$ slider-ice contact regions, each of size $a$, assumed that viscous shearing of the water film at each contact generated the frictional heat, and assumed that transient heat conduction governed heat flow into both bodies. They also iteratively included water loss by squeeze-flow to reduce $h$. A major assumption was that each contact was a constant, 1-mm square, with $n$ increasing with normal load such that normal pressure in each contact equaled $H_i$. This resulted in $\mu \propto n^{-1/2}$. Here, a concern is that $\mu$ depends fairly strongly on the choice of $a$, and 1 mm seems much too large to represent slider asperities. As with other self-lubrication models, the Makkonen and Tikanmäki model predicted very thin water films: $h < 0.1$ μm for 1 m s$^{-1}$ speeds at temperatures below −2°C. They did not note the difficulties such thin films pose to the formulation.

Lozowski and Szilder (2013) and Lozowski et al. (2013) formulated a friction model for speed skates that included crushing and self-lubrication components. They assumed that the blade crushed ice at constant pressure, equal to drop-ball
hardness (Poirier et al., 2011), to support the skater’s weight. The model calculated the crushing power dissipated, but it did not consider the role of the crushed particles along the interface and instead assumed that a hydrodynamic film began at the front of the contact zone. The formulation included squeeze flow but neglected heat flow into the skate blade. Overall, the model gave excellent agreement with measured speed-skate friction (De Koning et al., 1992), including variations caused by blade tilt during actual skating strides. However, the model predicted $h < 0.5 \mu m$ for $v < 12 \text{ m s}^{-1}$ at $-5^\circ \text{C}$, with thinner films at the front of the blade and at lower speeds and temperatures. Although Lozowski and Szilder (2013) noted that polished front of the blade and at lower speeds and temperatures.

Researchers have also proposed that self-lubrication can account for low friction on snow despite important mechanical and structural differences with ice. The front of a slider simultaneously compacts and shears natural snow. Even well-sintered snow can deform and fail in response to frictional shear before contact points warm to $0^\circ \text{C}$. Assuming persistent snow-grain contacts form, real contact area must increase during sliding either by melting or abrading contacting grains. This process is central to quantifying snow friction but is largely unknown and potentially quite different from contact evolution on ice. If meltwater films form, pore spaces in snow allow water loss through squeezing, shearing and plowing by slider asperities, processes also very different from those on ice.

**Self-Lubrication on Snow**

Colbeck (1988), Colbeck (1992) attributed to Klein (1947) the concept of three snow-friction mechanisms: solid-solid, lubricated and capillary suction. Colbeck (1988) focused on self-lubrication, then Colbeck (1992) more thoroughly considered the role of other friction mechanisms. For self-lubrication, he envisioned grainscale (mm) lubricated contacts. At each of $n$ contacts (assumed equal in size), viscous shearing of the water film provided the heat to melt the grains and to conduct into the slider and the snow. He included two water-loss mechanisms: squeeze-flow from normal pressure and shearing-flow from slider forward motion, and argued that shearing-flow dominated. He treated heat flow into the snow grains as 1D transient conduction, and he considered several cases of heat flow into the slider: fully insulated, and transient, steady-state and periodic conduction, with the latter preferred qualitatively. The resulting model predicted $\mu \propto v^{-1/2}$ at low speeds and $\mu \propto v^{1/2}$ at high speeds, with high slider conductivity increasing friction at all speeds.

The model predicted $h < 0.1 \mu m$ for downhill-skiiing conditions ($v = 10 \text{ m s}^{-1}$, plastic ski) across the temperature range $-40^\circ \text{C}$ to $-0.5^\circ \text{C}$, assuming a relatively large grain-contact diameter of 2 mm (Colbeck, 1988). Because squeeze-flow rates increase as $d^{-2}$, smaller grain-contact areas would produce thinner films. Even after weakening the water-loss mechanism for hydrophobic sliders, Colbeck (1992) concluded that “... the calculated value for film thickness is probably too small to separate the solids under most conditions of interest, even when only squeeze occurs, and this suggests that there is solid-to-solid interaction as well as meltwater lubrication”.

Colbeck (1992) expanded his consideration of snow-friction mechanisms while cautioning that “... there is not enough information about them to combine them into a theory of snow friction for application.” He discussed surface properties of snow relevant to friction, the “polishing” effect of repeated passes, and noted that “... it is especially difficult to estimate the actual contact area during sliding.” He then introduced and discussed several snow-friction mechanisms: “plowing and compaction of snow in front of the slider, snow deformation below the slider, deformation or fracture of asperities, shearing of the water films that support the slider’s weight, capillary attraction from other water attachments, and drag by surface dirt.” He mentioned but did not treat snow disaggregation (i.e., grain-bond failure) as a mechanism, noting that it “... might be important since snow grains seem to release by rebound after rapid ski passage.” To add to this daunting task, Colbeck noted that these mechanisms often interact.

Colbeck (1992) extensively discussed dry contact mechanics and the transition to melt-water lubrication, and he noted that lack of important details impedes understanding of dry-contact friction. To estimate the relative importance of the two, he predicted the dry-contact length, $L_d$, to raise the snow ambient temperature to $0^\circ \text{C}$, based on Eq. 6 and assuming an insulated slider:

$$L_d = \frac{\pi k^2 T_0 (A_i/A_s)^2}{4 K \mu v^2 d_t}$$

where $T_0$ is snow ambient temperature, and $p_s$ is slider nominal pressure. Heat flow into the slider increases $L_d$. The predicted length depends strongly on the actual contact area and the dry-contact friction coefficient, $\mu_d$, both assumed to be constant. However, dry-contact abrasion should increase $A_s$ as grains wear, and many friction studies indicate that $\mu_d$ can initially be quite low and increases as the slider shears snow-grain or ice asperities. These changing conditions invalidate the assumptions embedded in Eq. 8. Furthermore, if the slider fails the snow intergranular bonds and the grains move, persistent heating does not occur. That is, Eq. 8 may not provide reasonable predictions for the dry-contact length under a slider and thus the relative importance of dry vs. lubricated friction mechanics. Also, Colbeck’s self-lubrication model assumed that $nd^2 = const$, so that the size of each contact would reduce as more grains came into contact. This seems counterintuitive, as both the size and number of contacts should increase as the slider melts or abrades the contacting grains.
Lehtovaara (1989) developed a similar self-lubrication model for ski-snow friction but neglected heat flow into the ski. He also derived Eq. 8 to estimate the length of the dry-contact region. Lehtovaara included only squeeze flow (no shear flow) to account for water loss at the contacts, but did describe mixed dry/lubricated friction, with a transition to fully lubricated at $h > 3 R_n$, half of the value recommended by Bhushan (2013; Eq. 7c). Wet friction followed Eq. 4, and the dry-friction coefficient was assumed to be 0.06. To assess the model, Lehtovaara tested short sliders against flat ice using a rotary tribometer. He allowed a long (3 km) run-in distance for each test specimen “... to ensure that a steady-state friction process was achieved.” Interestingly, measured roughness of each slider decreased during the tests, suggesting that dry-contact polishing was an important process.

Bäurle et al (2007) formulated a numerical model for sliding on ice and snow that included dry and lubricated contact. Importantly, they attempted to account for the evolution of real contact area as sliding progressed. After compacting snow samples, they measured static contact areas ($A_i/A_n \sim 0.01–0.1$) using micro-computed tomography. They also used scanning electron microscopy (SEM) to examine the surface of snow samples subjected to repeated passes of a small ski and suggested that the flattened grain contacts showed evidence of melting. The model assumed constant dry-contact friction ($\mu_d = 0.3$) at the start of sliding until the water film thickened sufficiently to equal that friction, after which the model used wet friction. In its full form, their self-lubrication model included heat flows into both surfaces and water loss by squeeze flow. They accounted for 3D heat transfer at the contact areas by altering ice thermal conductivity with contact-area ratio, although most researchers view 1D heat flow as a reasonable assumption at sliding contacts (Blok, 1937; Archard, 1959; Carslaw and Jaeger, 1959). They also heuristically attempted to account for slider roughness, although they did not treat its effect of increasing squeeze-flow (Moore, 1965). Nevertheless, the model posed a fairly complete implementation of self-lubrication theory for snow.

In lieu of testing on snow, Bäurle et al (2007) measured friction and surface-temperature rise of a 40-mm-long polyethylene slider pressed against a rotating ice ring. Their data and numerical results revealed several interesting features:

- Measured friction coefficients (shown for $-5^\circ$C) started below $\mu = 0.007$ and smoothly rose to $\mu \sim 0.053$ after 1 s of sliding before increasing more gradually.
- Even after 10 s of sliding, measured interface temperatures were below $-2^\circ$C near the front of the slider and below $-3^\circ$C at the center and rear of the slider. The model also predicted average interface temperatures below $-2^\circ$C.
- Predicted $h$ increased along the slider but remained below 0.25 $\mu$m at $-5^\circ$C and 1.3 $\mu$m at $-0.5^\circ$C ambient temperatures. The roughness of the slider was $R_n = 2 \mu$m.

The very low starting friction probably resulted from shearing of ice asperities (dry-contact), and the thin predicted films relative to slider roughness suggest that dry or mixed contact probably occurred throughout the tests. Measured sub-freezing interface temperatures are consistent with dry-contact abrasion (see Abrasion and Dry Lubrication), so lubricated contact may not have governed their tribometer tests.

**Summary of Self-Lubrication**

Self-lubrication, the prevailing hypothesis for the slipperiness of ice and snow for over 80 years, has some significant shortcomings despite offering helpful insights. On both ice and snow, the supporting water films must be substantially thicker than the combined roughness of the surfaces, a test that most self-lubrication models fail. Many studies have overlooked or poorly represented slider topography and roughness and their influence on interface mechanics. For sliders on ice, many studies have observed abrasion of the sliders and ice surfaces but have not described the mechanics of transition from dry to lubricated contact. For sliders on snow, it is difficult to rationalize persistent heating and melting of contacts owing to snow’s susceptibility to intergranular bond breakage and movement during sliding. On both substrates, lower startup friction compared with steady-state friction suggests that hydrodynamic lubrication may not be the slipperiest friction mode. These issues warrant more attention if self-lubrication is to continue as the prevailing theory.

**Quasi-Liquid Layers**

Surfaces are inherently disordered, with unsatisfied bonds that present a higher-energy state than the bulk substrate. Species from the surrounding environment readily adsorb to surfaces to lower the overall system energy. This process is inherently dynamic and can involve ongoing rearrangements of the surface atoms or molecules as well as exchanges with the adjacent phase (Myers, 1991). Ice surfaces are no exception.

**Quasi-Liquid Layers on Ice and Snow**

Water molecules on ice and snow surfaces have properties intermediate to those of the bulk ice and liquid: unsatisfied hydrogen bonds cause the surface water molecules to be more mobile than those within the bulk ice (Glen, 1968; Neshyba et al., 2009; Loudon and Gezelter, 2018; Weber et al., 2018; Nagata et al., 2019), imparting liquid-like properties at the molecular scale. A quasi-liquid layer (QLL) on ice, at temperatures below the bulk-melting point, can reduce surface energy at a vapor or solid boundary. The layer thickness represents an energy minimum, balancing energy to melt the layer with the reduction in surface energy (Dash et al., 1995; Dash et al., 2006).

Recent advances in measurement techniques and molecular-dynamics simulations (MDS) have provided remarkable insight into the nature and emergence of QLLs on the surface of ice. These efforts show large variations in QLL thickness vs. temperature, but values generally vary from a few nanometers near $-40^\circ$C to tens of nanometers near $0^\circ$C (Doppenschmidt and Butt, 2000; Pittenger et al., 2001; Rosenberg, 2005; Li and Somorjai, 2007; Slater and Michaelides, 2019). Paesani and Voth (2008) conducted MDS using a quantum-mechanical, rather than classical, model of water molecules and concluded that quantum effects can account for some discrepancies between measurements and predictions of QLL thickness.
Different regimes of QLL appear to exist. Sazaki et al. (2012) used advanced, laser confocal microscopy combined with differential interference contrast microscopy to observe the emergence of two immiscible phases of QLLs, droplets and thin films, directly on the surface of ice at temperatures $-1.5$–$0.1^\circ$C. Nagata et al. (2019) summarized the transition of homogeneous disordered surface layers, an equilibrium process that begins at about $-90^\circ$C, through to the emergence of inhomogeneous, non-equilibrium QLL droplets and films near the bulk-melting point.

**Quasi-Liquid Layer Role in Ice Friction**

Weber et al. (2018) provided direct evidence that QLLs can play an important role in ice friction (Figure 5). They combined MDS with steel sphere-on-ice friction tests to reveal a strong correlation of measured friction with calculated surface mobility (diffusion) of water molecules over the temperature range $-10^\circ$C to $-100^\circ$C and sliding speeds $10^{-6}$–$10^{-1}$ m s$^{-1}$. The Arrhenius dependence (exponential-decay) of measured $\mu(T)$ below about $-7^\circ$C had the same activation energy as the lateral self-diffusion constant of surface water molecules from the MDS, $\sim 11.5$ kJ mol$^{-1}$ or about 1/2 of the hydrogen-bonding energy. This correlation encouraged them to conclude “... that slippery ice arises from the high mobility of its surface molecules, making the ice surface smooth and the shearing of the weakly bonded surface molecules easy.” Weber et al. (2018) also found that friction was independent of sliding speed for tests at $-7^\circ$C and $-12^\circ$C, which they interpreted as indicating that “... frictional heating does not play an important role in the experiments.”

Louden and Gezelter (2018) used MDS to map the reduction in viscosity of the QLL molecules with distance from the bulk substrate and agreed with Weber et al. (2018) “... that the small coefficients of friction commonly associated with ice surfaces are due almost entirely to the shear viscosity of water molecules near the QLL/vapor interface.” Nagata et al. (2019) went further to suggest that “... the disordering of the topmost ice surface governs the slipperiness of the ice surface, allowing for ice skating” and that “The observation of velocity-independent friction is inconsistent with the frictional melting hypothesis...”

Despite identifying an important ice-friction role for QLLs, Weber et al. (2018) also showed that deformation of the bulk-ice substrate played a role in their tests. They modeled ploughing of the steel sphere through the ice as a plastic-deformation process at pressures equal to separately measured $H_f(T)$. This ploughing term accounted for their measured rise of friction near $0^\circ$C.

Lieberink et al. (2021), expanding on Weber et al. (2018), clarified the role of ice deformation on measured friction. Testing spheres of differing roughness and normal load, friction from ploughing became important above $\sim -20^\circ$C as contact pressures, including from increased roughness, exceeded measured hardness. Indeed, rms roughness played a role above $R_q \sim 0.2$ µm, even for ice at $-50^\circ$C, and the roughest sphere ($R_q \sim 3$ µm) left µm-deep striations in the ice. Clearly, the QLLs did not prevent direct ice contact by slider asperities. Also, Liefferink et al. (2021) measured a non-monotonic velocity-dependence of friction at $\sim -20^\circ$C, which they attributed to velocity effects on penetration hardness and thus ploughing friction. They noted that the ice substrate responded elastically in the low-temperature region that displayed the diffusion-correlated Arrhenius dependence of $\mu(T)$, and that “... friction on ice increases exponentially with the local contact pressure, suggesting that this pressure frustrates the mobility of the lubricating layer.”

Bluhm et al. (2000) measured friction on ice of $\mu \sim 0.6$ over temperatures $-24^\circ$C to $-40^\circ$C using an atomic-force microscope tip scanned at 5 µm/s. They concluded that the tip moved sufficiently slowly to displace the quasi-liquid film and consequently measured dry friction. This result also indicates that the QLLs did not continuously reform under the tip, and may not reform under slider asperities, to facilitate low friction.

**Quasi-Liquid Layer Summary**

The high mobility of QLL water molecules can account for the slipperiness of ice provided the bulk substrate responds elastically. However, the results of Weber et al. (2018), Liefferink et al. (2021) and Bluhm et al. (2000) limit the role of QLLs on ice friction: QLLs do not prevent macro-scale deformation of the bulk-ice substrate, and micron-scale slider asperities can directly gouge the substrate. Depending on slider geometry, normal load and speed, bulk-ice brittle crushing could occur. Importantly, rapid micron-scale asperity interactions should induce local brittle failure and thus generate wear particles. Crushed ice and wear particles could play important roles in ice-slider interaction despite the presence of QLLs.

![Figure 5](Image 144x586 to 451x712)
Abrasion and Dry Lubrication

Abrasion and wear are ubiquitous on unlubricated sliding surfaces. The extreme brittleness of ice makes it susceptible to brittle wear by slider asperities or fracture at ice and snow-grain asperities. Bulk-snow intergranular bonds are also susceptible to brittle fracture, allowing the grains to move in response to slider shear. These processes could prevent warming and melting of persistent contacts (self-lubrication) and limit the role of nano-scale QLLs to govern friction. Here, we summarize theory and evidence that dry-contact abrasion and wear could play important roles in ice and snow friction (Figure 6).

Abrasion on Ice

Akkok et al. (1987) formulated a simple model that considered the flash-temperature rise (Blok, 1937; Archard, 1959) for a contact sliding on flat ice or for an ice contact sliding on a flat material. They solved for the friction coefficient that would cause the contact temperature to rise to an upper-bound temperature, $T_f < T_m$ and explained that “Essentially $T_f$ must be that surface temperature above which the material at the immediate surface cannot remain in the contact since it is easily abraded and removed by shear.” Similar to Evans et al. (1976), this approach allowed them to predict friction coefficients and their variations with system parameters without identifying the friction mechanism, except to note that it was not viscous shearing of a melt-water film. They then compared model predictions with their own friction measurements and those of Evans et al. Quantitative agreement was not strong, but the model predicted the dominant speed effect, $\mu \propto v^{-1/2}$. This dependence falls out of the assumption of transient heat-conduction into the ice by combining Eqs (4-6) with $t = l/v$, where $l$ is slider length:

$$\mu = \frac{\Delta T_f l}{2\sigma} \left( \frac{\pi}{K l v} \right)^{1/2} \quad \text{(9)}$$

An important assumption embedded in Eq. 9 is that $\mu$ (or heat flux $q_f$) is constant, which may not be true along a slider as friction mechanics and contact area change. However, the general $\mu \propto v^{-1/2}$ does not require that $\Delta T_f$ raise the ice temperature to melting or that friction results from viscous shearing of a water film.

Tusima (2011) formulated a dry-contact model for ice friction, $\mu = \tau/\sigma$, with $\tau$ attributed to adhesion between the ice and the slider. The model correlated well with ice-friction tests by adding a ploughing term to the shear stress. These were mostly low-speed tests ($7 \times 10^{-5} \text{ m s}^{-1}$) where plastic yielding of the ice could have governed its behavior for both the adhesion and ploughing terms. Nevertheless, Tusima photographed tracks left by the spherical sliders that showed striations and noted abraded particles, recrystallization and cracks, with higher $\mu$ correlating with more surface damage. Importantly, he measured lower friction on ice basal planes compared with prism planes, which he attributed to lower shear strength and higher normal strength on basal planes. Tusima (2011) reported similar reductions in friction of speed-skate blades at $\sim 1 \text{ m s}^{-1}$ on an ice rink consisting entirely of basal-plane ice ($\mu = 0.0038$) compared with polycrystalline ice on a standard rink ($\mu = 0.0045$), although the slightly colder polycrystalline ice could have accounted for some of the difference. He concluded that the dependence of ice friction on crystallographic plane supported his theory of pure solid friction without lubrication from melt-water.

Makkonen and Tikkanmäki (2014) formulated a dry-contact ice-friction model to supplement their self-lubrication model. They related friction in the dry-contact regime to the change in surface area at a nano-scale sliding contact:
\[
\mu = \frac{Y + Y_s - Y_{sd}}{2dH_i}
\]

where \(Y\), \(Y_s\), and \(Y_{sd}\) are the surface energies of the ice, slider and ice-slider interface, respectively, and \(d\) is a characteristic nano-scale contact length, assumed to be 2 nm. A concern with this formulation is that the surface area of ice created during dry-contact sliding should include any wear particles formed by brittle failure at the asperities, which would increase the area associated with the \(Y\) term. The selection of \(d = 2\) nm also differs from the contact length for their wet-contact model (1 mm) with no discussion of the mechanics of transition between the two.

**Abrasion on Snow**

Lever et al. (2018) sought to document the transition from dry to lubricated contact for a ring of polyethylene sliding on compacted snow, using a high-resolution IR camera to measure evolving snow-grain contact area and temperature. Unexpectedly, they obtained evidence that contradicted self-lubrication theory. Measured friction was low (\(\mu < 0.03\)) for cases where slider shear caused widespread intergranular bond failure with no persistent contacts to melt. When the snow grains did not move, the slider abraded but did not melt the evolving contacts yet still produced low friction (\(\mu < 0.05\)). Lever et al. (2019) obtained additional evidence that abrasion could govern snow friction by coordinating IR, optical microscope and SEM images of the contacting snow grains. IR thermography again showed no melting, while coordinated images revealed that wear particles abraded from stationary grains deposited and sintered together in the snow’s pore spaces to produce lacy structures that could completely fill the pore spaces to the plane of the slider.

Lever et al. (2019) formulated a partial snow-friction model based on dry-contact abrasion and heat transfer to account for and extend their observations. They applied the Archard (1953) model of abrasive wear, and it reasonably predicted the evolution of snow-grain contact area. They also applied an extension of sliding-heat-source theory (Tian and Kennedy, 1993; Tian and Kennedy, 1994) to account for multiple contacts sliding across finite bodies, which predicted that contact temperatures would not reach 0°C during their tribometer tests. Importantly, the thermal model predicted that flash temperatures would be small on typical 10–100 μm-diameter snow-grain contacts. Consequently, they asserted that existing field measurements of interface temperatures on skis and sleds closely approximated actual contact temperatures. Measurements on skis (Colbeck and Warren 1991; Colbeck and Perovich 2004; Schindelwig et al., 2014) and sleds (Lever and Weale 2012; Lever et al., 2016) have consistently shown that interface temperatures remained well below 0°C under the action of sliding friction. Self-lubrication may not occur for sliders on snow at common field conditions.

**Abrasion and Dry-Lubrication Summary**

Lever et al. (2019) suggested that dry-contact abrasion and heat flow can prevent the formation of lubricating water films for snow-friction scenarios of practical interest and speculated that the wear particles could serve as a dry lubricant to account for why snow is slippery. Third-body tribology theories attempt to account for the production, loss and shearing of wear particles at sliding interfaces (Godet, 1984; Iordanoff et al., 2002; Fillot et al., 2007), and these ideas could guide formulation of dry-lubrication theory for ice and snow. One mode of dry lubrication is that a layer of fine wear particles can act as a viscous fluid (Heshmat, 1991; Heshmat, 1995; Wornyoh et al., 2007). However, Lever et al. (2019) did not directly observe the presence of wear particles at the contacting interfaces owing to their small size and rapid post-test sintering. Thus, this dry-lubrication hypothesis remains unproven, and it is unclear whether it plays an important role in ice friction, where abraded particles may be trapped at the interface and melt under further sliding rather than deposit into voids between snow grains.

**Ice-Rich Slurries**

Ice-rich slurries can form beneath an indenter during rapid indentation of ice (see Ice Indentation), including with concurrent sliding motion. It is also possible for ice-rich slurries to form by sliding friction, as abraded wear particles partially melt (Figure 7). The viscoelastic properties of the resulting slurry film could account for why ice and snow are slippery, with dry and fully liquid lubrication as the two end states based on the film’s water content.

**Ice Friction With Micro-scale Ice-Rich Slurries**

Gagnon and Molgaard (1989) measured kinetic friction with concurrent crushing of freshwater ice against a rotating steel wheel. Crushing rate was constant at 5.5 mm s\(^{-1}\), temperatures ranged \(-5°C\) to \(-19°C\) and sliding speeds 0.06–0.82 m s\(^{-1}\). Friction during crushing was generally low (\(\mu \sim 0.02–0.1\)) and decreased with increasing temperature or wheel speed. The tests produced periodic crushing and extrusion of pulverized ice, similar to ice-indentation tests without sliding motion. Video records revealed mm-thick layers of pulverized ice at the contact zone along with some melt-water.

Gagnon and Molgaard (1991) and Gagnon (1994a), Gagnon (1994b), Gagnon (2010) conducted follow-up ice-indentation tests that revealed important features relevant to crushing-friction mechanics: isolated HPZs of intact ice could apply pressures approaching the melting pressure; micron-scale ice-rich slurries (liquid content <20%) existed at the interfaces between HPZs and the slider/indenter; these HPZs could support nearly 90% of the normal load; energy expended in the viscous squeeze-flow of the slurries could consume >60% of the mechanical work supplied by the system.

Returning to ice friction, Gagnon (2016) crushed ice against high-roughness surfaces with concurrent sliding motion. Tests were at \(-10°C\) and covered a range of crushing and sliding rates \(\sim 4–30\) mm s\(^{-1}\). Friction coefficients were remarkably low (\(\mu \sim 0.02–0.14\)) given the mm-scale surface roughness. High-speed video identified ice-rich slurries separating the intact-ice zones from the contacting slider elements. Pressure across the slurries reached 55 MPa, or about half of the pressure-melting value. Gagnon suggested that the formation and extrusion of ice-rich slurries controlled the friction mechanics: “The squeeze-film
slurry dissipates the majority of the actuator energy supplied to the system because the load is mostly borne on the hard-zone ice (∼88%, Gagnon, 1994a), where the slurry is generated and flows.” He noted that “The layer may be thought of as a self-generating squeeze film that is powered by the energy supplied by the loading system that causes the ice crushing.” Gagnon noted that these processes should be considered to explain the friction on ice of skate blades, sled runners and curling stones, where ploughing or local crushing of ice asperities occurs. He also noted that high-roughness surfaces such as tracks or wheels could unexpectedly experience low friction on ice when crushing occurs.

**Ice Friction With Sub-micron Ice-Rich Slurries**

Canale et al. (2019) measured the nano-scale tribology and rheology of ice-slider interfaces using a novel “stroke-probe” tribometer consisting of a mm-scale smooth glass bead ($R_q \sim 0.4$ nm) mounted to a double-mode tuning fork. Horizontal vibration against the ice revealed the frictional behavior, and vertical vibration during retract of the probe revealed the rheological behavior of the interfacial film. Tests covered 0°C to −16°C with peak oscillatory speeds to 0.09 m s$^{-1}$. Each test began with a run-in period after reaching the target normal force, during which the friction force steadily increased, indicating some development of the interfacial film. The authors noted that “… during the retract the normal conservative impedance does not exhibit a square root dependence with the indentation as it would be expected for a Hertzian deformation; it rather exhibits a hydrodynamic behavior, pointing to a fluidized interface.” Friction varied as $\mu \propto v^{-\gamma}$ with $\gamma \sim 0.3$–0.5, in common with many macro-scale tests, and was independent of normal load, suggesting solid-like friction behavior with $\mu \sim 0.015$. Friction and film thickness both increased with temperature above −10°C, with $h$ ranging 0.1–0.4 μm.

Canale et al. (2019) measured lubricating films that were much thicker than QLLs and displayed viscoelastic behavior, with viscosity up to two orders-of-magnitude greater than liquid water. Higher normal loads produced greater viscosity, and extrapolation of measured viscosity to zero normal load matched the viscosity of supercooled water at the test temperature. Elastic modulus averaged about 100 Pa. They suggested that the high viscosity of the film “… points to an unexpected rationale for the exceptional friction properties of ice, contrasting with the bad lubricant behavior of bare liquid water. Indeed, a viscous film is a prerequisite to properly lubricate the contact: it limits squeeze-out, thereby avoiding direct solid-on-solid contact.” They concluded that “… a tempting explanation for the observed response is accordingly that, under abrasive wear, a suspension of liquid and submicron … debris is formed, hence resulting in composite lubrication of the contact.” The observed increase in friction and viscosity with temperature “… may be interpreted as an increasing density of ice fragments when the ice becomes softer close to the melting point.”

**Summary of Ice-Rich Slurries**

Ice-rich slurries can result from crushing or abrasion by slider motion, with water fraction dependent on confining pressure and heat generated by shearing of the particle layer. Ice-rich slurry films could potentially form on both ice and snow substrates, and their high viscosity and elastic properties could separate and lubricate the slider. The mechanics of such slurries could explain how dry contact at the front of a slider transitions to fully lubricated contact and help to map the regimes where each end state governs system friction.

**EVIDENCE OF ICE- AND SNOW-FRICTION MECHANICS**

Researchers have undertaken tribometer studies on ice and snow for various purposes: to investigate the underlying mechanisms,
to understand the role of system properties, or to minimize (e.g., winter sports) or maximize (e.g., vehicle tires) friction. Test variables include slider geometry (e.g., flat, spherical) and motion (e.g., unidirectional, reciprocating) plus slider material properties, ice crystal structure or snow morphology. Given these differences, it can be difficult to compare tribometer results or to infer underlying mechanics using only the dependence of $\mu$ on system variables.

A fundamental difficulty is that the friction mode (dry, boundary, mixed, lubricated) can vary with position along a slider and duration of sliding. The existence of different modes introduces a scaling requirement not generally acknowledged for laboratory ice- and snow-friction tests: to isolate and separately scale the contributions from each mode to extrapolate to full-scale systems (Glenne 1987; Colbeck 1992). Nachbauer et al. (2016a) and Hasler et al. (2016) developed a 24-m-long linear tribometer to test full-scale skis in part to avoid this scaling requirement. Nachbauer et al. (2016b) highlighted systematic variations in friction along a ski by testing sliders of increasing length.

Another difficulty involves the common use of a “run-in” period to seek steady-state conditions. As noted, friction on ice and snow often rises from very low levels during run-in. If the goal is to understand why they are slippery, it seems counterintuitive to omit the slipperiest portion of the tests. Also, the field application matters: for skis, sleds, tires and other systems of interest, the ice or snow experiences brief, one-pass contact by the slider. The substrate’s initial response should be of particular interest, and the friction mechanics could be quite different from those governing after repeated passes (Hsia et al., 2020).

We summarize here evidence of the mechanics underlying ice and snow friction obtained through direct observations, beyond efforts noted in Postulated Ice and Snow Friction Mechanisms.

Evidence of Ice-Friction Mechanics

Tusima and Yoshida (1969) continuously rotated a disc of ice against a thick ring of acrylic. They intentionally ran long-duration tests and observed water droplets flying off the disc after 30–60 s at 10.5 m s$^{-1}$ and ~35°C. They estimated film-thickness of 10–50 μm for these tests. At 0.155 m s$^{-1}$ and warmer temperatures, they observed transparent, nm-scale spots rotating with the ice, which they interpreted as melt-water at the real-contact areas. The size of the spots decreased with decreasing temperature, and they did not observe spots below ~15°C. Although they suggested that the melt-layers formed right away, a plot of friction force at 10.5 m s$^{-1}$ and ~19°C showed ~1 s rise from very low values followed by a slow decrease. If the rise occurred at constant normal load, initial dry-contact produced lower friction. Also, abrasion can polish ice contacts and may have produced the transparent spots observed during the low-speed tests. If the spots had been melt-water films, Tusima and Yoshida should have seen smearing in the direction of motion, but none was reported.

Strausky et al. (1998) used fluorescence spectroscopy to measure water-layer thickness separating an acrylic slider on a rotating ice disc. Contact pressure was 5 MPa and speed ranged 0.005–0.1 m s$^{-1}$. After ~60 s of run-in, they measured $\mu = 0.03$ at ~2°C but observed no water films thicker than their detection limit of 50 nm. They noted that this result “... supports some suggestions in the literature, in which the interface is described as ... a liquidlike layer being several hundred molecules thick”. Indeed, these findings could support the QLL hypothesis, although Weber et al. (2018) and Lieferink et al. (2021) found that ploughing dominated friction at ~2°C. Alternatively, the lack of a detectable water film could be consistent with abrasion/dry-lubrication or the ice-rich slurry hypothesis, depending on the sensitivity of the spectrometer to low water fraction in a slurry.

Marmo et al. (2005) used a reciprocating linear tribometer to generate a friction map of ice hemispheres sliding against steel. The map plotted 449 friction values spanning ~27°C to ~−0.5°C, 0.008–0.37 m s$^{-1}$ and two normal loads. They used 60-grit silicon-carbide paper to finish the steel surface, which suggests $R_n \sim 2–3$ μm. They conducted companion tests to obtain specimens for low-temperature SEM imaging of the wear surfaces in three regimes of the friction map. The resulting images show fine detail in the wear surfaces and adjacent debris bands. They carefully described features suggesting refrozen melt-water on the two specimens that produced low friction ($\mu = 0.06–0.07$), for example: “... concave grooves in the wear surface separated by sausage-shaped ridges that display no evidence of brittle deformation ... The grooves are filled with fine, rounded interconnecting ridges that appear to be the remnants of liquid water.”

Conversely, they describe features of the high-friction sample ($\mu = 0.16$) consistent with dry contact: “The worn surface shows signs of brittle deformation with microcracks and scuffing ... Scuffing is a common wear morphology produced by failure when the sliding interfaces become welded together ...”

While it can be difficult to link SEM-observed features unambiguously to processes, Marmo et al. (2005) stated their interpretations clearly. The images show striations from the rough steel surface, so mixed-mode friction was likely even if liquid formed at the wear surface. The authors calculated water-film thickness as (0.88–6.97) x 10$^{-11}$ m for the low-friction tests (via Eq. 4 here). These values are thinner than the diameter of a water molecule (~0.3 nm). Perhaps the evidence of refrozen liquid related to QLLs rather than micron-scale melt-films, but that raises the question of how it could be observed hundreds of microns away from the wear surface. Studies that couple SEM with other diagnostic modes could help resolve these issues.

Higgins et al. (2008) pressed ice hemispheres against a rotating disc of rubber and produced a friction map consisting of 225 measurements spanning ~33°C to ~−1.0°C and 0.003–2.6 m s$^{-1}$. They also conducted five similar tests to provide samples for SEM imaging using the same methods as Marmo et al. (2005) and clearly stated their interpretations of features linked to dry and lubricated contact. For example, they described evidence of dry-contact friction at ~−25°C and 0.005 m s$^{-1}$ that produced $\mu = 0.85$: “The smeared, multi-layered features ... demonstrate successive layers of this slurry mixture being deposited at intervals during sliding and indicate deformation of entrained ice debris.” Interestingly, for two tests at low speeds that produced the same friction ($\mu = 0.30$), they described features that suggested melt-water formation at ~−5°C and dry-contact friction at ~33°C. They also identified melt-
features for a −20°C test (μ = 0.35, 2.1 m s⁻¹): “The wear surface shows signs of melting with “sausage-shaped” ridges present, identified in Marmo et al., 2005 as being formed by refreezing of liquid.” These diagnostic efforts suggest that friction mechanisms can change significantly yet produce similar friction values. For the lubricated-friction cases above, Eq. 4 would predict h ∼ 0.2–50 nm, which again are too small to be realistic water films. Mixed-mode friction was likely.

Klein-Paste and Sinha (2010) examined ice surfaces before and after single-pass, short-duration (~40 ms) sliding by rubber. They used a traditional etching and replicating technique to create thin-plastic casts of the ice surfaces that revealed grain boundaries, dislocations, and “... most importantly, deformation related features like tilt boundaries, dislocation cells and pileups.” For all tests, the casts captured ploughing tracks and rows of dislocation etch pits consistent with deformation by the rubber slider. They saw no evidence of melt-water even for tests at −0.1°C and high-speed sliding (3 ms⁻¹) that produced low friction (μ = 0.08). They suggested that their results contradicted Higgins et al. (2008) owing to the longer duration (15 s) sliding used in those earlier tests. Although they allowed that etching could have removed very thin water layers (<0.1 μm), they noted that ice deformation occurred even close to the melting point and that “…deformation processes during ice friction are not strictly confined to viscous shearing of a melt water film at the interface.” As a minimum, mixed-mode friction occurred.

Tuononen et al. (2016) sought to clarify the mechanics of rubber-ice sliding via observations guided by multi-scale friction theory (Persson, 2015). They conducted repeated, unidirectional sweeps of rubber on ice and measured the resulting changes in surface topography at three magnifications using white-light interferometry. Even after the first sweep (~0.3 m long), they observed scratches in the ice surface at the lowest magnification, which they attributed to silica filler particles in the rubber. The number of scratches increased with the number of sweeps. They used the number of scratches and their average cross-sectional area to determine that ploughing friction was a negligible contribution, with viscoelastic energy dissipation of the rubber and heat flow into the ice contributing about equally to the measured friction.

At the highest magnification, Tuononen et al. (2016) observed isolated droplets of refrozen water, similar in dimensions to the QLL droplets observed by Sazaki et al. (2012) but aligned with the direction of sliding, “... which indicates that the meltwater freezes relatively quickly, or is only in a quasi-liquid state.” They also noted “No ‘sausage-shaped’ meltwater features ... were observed ...” Also, “The droplets ... may originate from melted virgin ice asperities and/or from a liquid-like layer of premelted ice which may become more liquid-like as a result of the frictional heating of the ice surface.” Interestingly, at the start of the first sweep, friction increased from low levels to a maximum after ~1 mm of sliding. They argued that the subsequent decrease was “… at least in part, related to frictional heating and the softening or melting of the ice in the asperity contact regions ...”. This work makes a convincing case for the need to consider ice friction as different processes acting on different spatial and temporal scales.

**Evidence of Snow-Friction Mechanics**

Huzioka (1962) continuously rotated a glass disc against a block of compacted snow, and from microphotographs taken after 5 min of sliding (69 mm s⁻¹, −4°C and 4.6 kPa), measured the area of the 190 contacting grains as 1.4% of the nominal area. Huzioka (1963) conducted similar experiments that revealed differences in contact mechanics for glass and acrylic discs. For snow against bare glass (~2°C for 5 min), “The glass plate rubbed off the projections of the ice grains of snow and left scobs (ice particles) to the right (downstream) side of the actual contact areas.” When the glass was coated with a film of lacquer, “… the actual contact areas became wider and more scobs were produced. ... Almost all the ice grains are rubbed off and the spaces between them are filled up by the scobs.” The respective friction coefficients were μ = 0.30 and 0.13 for the bare and lacquer-coated glass. Apparently, the higher rate of dry-contact abrasion reduced sliding friction. Conversely, when the snow was rubbed by acrylic, the microphotographs showed “... ice sticks extending in the direction of motion” from several contacting grains, consistent with refrozen melt-water. Huzioka (1963) reported μ = 0.61 for this test, noting that the higher friction contradicted the belief that meltwater plays the role of a lubricant. Kuroiwa (1977) noted that these microphotographs also showed “filings” (i.e., wear particles) produced by friction, indicating mixed-mode contact.

Ambach and Mayr (1981) used a capacitive probe to measure the thickness of water films between a ski and snow during downhill skiing. They calibrated the probe using static measurements of waterfilm thickness. Two runs of varying speed 0–17 m s⁻¹ on −5°C and −10°C snow gave film thickness ~4–20 μm, with thickness increasing with speed down the course. A run at constant speed on alternate sections of piste (compacted snow) and deep snow showed thicker films on the deep snow. This casts some doubt on the measurements, because snow grains fracture and move down-track under the action of a ski on natural snow (Nakaya et al., 1936; Kuroiwa, 1977), reducing the opportunity for friction to warm and melt persistent contacts. Also, modeling by Colbeck (1988) and Bäurle et al. (2007) predicted film thickness less than 1 μm for skiing conditions. It’s possible that friction-generated electric charge (Petrenko and Colbeck 1991) affected the Ambach and Mayr capacitive probe.

Lever et al. (2019) demonstrated that, for realistic values of A/cm², flash temperatures on snow make small contributions, and thus nominal temperatures measured by flush-mounted thermocouples approximate snow-grain contact temperatures. Colbeck and Warren (1991) measured ski-snow contact temperatures on hard-packed snow that rose 3–5°C but remained well below 0°C. Interestingly, they measured the warmest contact temperatures on soft, fresh snow where intergranular bond failure would likely have impeded the formation of persistent contacts. Colbeck and Perovich (2004) showed that sunlight absorption can bring contact temperatures closer to 0°C, but ski runs at night raised contact temperatures from ~9.2°C to only -7.8°C. Lever and Weale (2012) and Lever et al. (2016) measured contact temperatures of flexible sleds towed at 2–3 m s⁻¹ over natural snow in Antarctica and Greenland. Towing resistance (dominated by sliding friction) dropped significantly with increasing contact temperatures, both during startup and at steady-state, but temperatures remained well below 0°C. The sleds also developed low steady-state friction, μ ~ 0.03–0.08, at ambient temperatures −5°C to −30°C. Overall, contact temperatures
measured to date contradict the self-lubrication hypothesis for skis and sleds on snow.

CONCLUSION

Why are ice and snow slippery? For the last 80 years, the prevailing hypothesis has been self-lubrication: rapid formation of a lubricating melt-water film by frictional heat arising from shearing of that film. However, it predicts water films that are too thin to separate surfaces with micron-scale roughness, and new diagnostic tools have revealed that sliders may not melt the ice asperities or snow-grain contacts despite low friction values. Importantly, an expectation that dry contact at the front of a slider transitions to lubricated contact warrants a description of the mechanics linking the two regimes: specifically, how does that transition occur? Furthermore, the mechanical behavior of the ice or snow substrate plays an important and largely overlooked role in governing the friction regime for practical systems.

The brittle behavior of ice and the weak bulk-strength of snow have not been included in most friction theories. Ice is brittle at temperatures close to its melting point and at strain rates relevant to most asperity and macro-slider interactions. Additionally, ice hardness is not a material property, and high-pressure zones accompanied by ice-rich slurries exist during combined indentation and sliding that influence the friction mechanics. The fracture of ice asperities, generation of wear particles, and their role as third bodies between the slider and the ice all warrant attention, preferably through observations at the sub-micron scale. It is possible that wear particles can act as dry lubricants to reduce sliding friction and prevent fully lubricating water films from forming except during long-duration, repeated sliding over the same ice substrate. When slider asperities interact with those on the ice, can pressure-melting, partial melt-water films or QLLs prevent fracture and generation of wear particles? This seems unlikely given the brittle behavior of ice.

Natural snow deforms easily, and even well-sintered intergranular bonds can fail in response to slider normal and shear stresses. The mechanics of snow friction should include the substrate’s response to these combined stresses, where the resulting snow-grain motion or asperity fracture can prevent persistent heating of contacts. Lift from pressurized porous flow under skis and snowboards, which reduces normal stresses at the contacts, also warrants more attention. The common test technique to “run-in” a snow substrate through repeated slider passes should be reconciled with the full-scale system of interest: does the full-scale slider encounter strong, compacted snow previously exposed to repeated passes, or does the slider engage the snow on a single pass that could deform and fracture it, locally or in bulk?

As instrumentation has improved, researchers have undertaken micro- and nano-scale observations of friction mechanics at ice and snow interfaces. Ample evidence reveals direct slider-ice contact in the form of slider abrasion, substrate striations, lines of nano-scale melt features, dislocation etch lines, sintered wear particles, etc. Even if melting or temperature-dependent softening occurs, most systems must experience mixed-mode friction with contributions that vary with contact duration and roughness-dependent pressures. While QLLs can govern ice friction when the substrate responds elastically, QLLs are too thin to prevent micron-scale asperities from directly interacting with the substrate.

Ice-rich slurries potentially offer a unifying hypothesis for ice and snow friction by relating the transition from dry to fully-lubricated contact through increasing water-content. Local crushing and dry-contact abrasion can provide the ice particles, and the slurry’s viscoelastic rheology can support and lubricate the slider. Such slurries can even support pressures sufficient to decrease the interface melting temperature by several degrees. Furthermore, QLLs would exist on the surfaces of ice wear particles and thereby establish the minimum effective water contact of a slurry. System characteristics and the duration of sliding would then govern the slurry’s spatial and temporal evolution.

Future high-resolution observations should aim to illuminate the actual contact physics occurring at interaction scales relevant to snow and ice friction. Researchers must somehow document the transitions in governing modes as contact temperatures increase with position along a slider or sliding duration, and then account for these varying modes when interpreting mechanics or scaling the results of tribometer tests to full-scale systems. These are demanding but necessary tasks to account for why ice and snow are slippery across systems of practical interest.

AUTHOR CONTRIBUTIONS

JL structured the review. JL, EA-S, ST, and AL all contributed to assessing hypothesized friction mechanics relative to available observations, with EA-S providing additional background on measurement and modeling techniques for quasi-liquid layers.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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