Search for a $Z'$ at the $Z$ resonance

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188
The search for an additional heavy gauge boson $Z'$ is described. The models considered are based on either a superstring-motivated $E_6$ or on a left-right symmetry and assume a minimal Higgs sector. Cross sections and asymmetries measured with the L3 detector in the vicinity of the $Z$ resonance during the 1990 and 1991 running periods are used to determine limits on the $Z-Z'$ gauge boson mixing angle and on the $Z'$ mass. For $Z'$ masses above the direct limits, we obtain the following allowed ranges of the mixing angle, $\theta_M$, at the 95% confidence level:

- $0.004 < \theta_M < 0.015$ for the $\chi$ model,
- $0.003 < \theta_M < 0.020$ for the $\psi$ model,
- $0.029 < \theta_M < 0.010$ for the $\eta$ model,
- $0.002 < \theta_M < 0.015$ for the LR model.
1. Introduction

The successful operation of LEP has allowed a precise measurement of the $e^+e^-$ annihilation cross sections near the $Z$ resonance [1,2]. The experimental results confirm the Standard Model [3] within percent precision. Nevertheless, the Standard Model may be regarded as the low energy limit of a theory which unifies electroweak and strong interactions at higher mass scales. Most of these theories predict additional heavy gauge bosons, $Z'$, and some models allow $Z'$ bosons with masses detectable at present or future colliders. A mixing of the $Z'$ with the standard $Z$ modifies the $Z$ couplings and changes the $Z$ mass. In addition, propagator effects of the $Z'$ deform the $Z$ resonance shape. Therefore, LEP is the ideal place to measure $Z$--$Z'$ mixing. Analyses [4] based on previous LEP data, on results of neutrino physics and atomic parity violation bound the $Z$--$Z'$ mixing angle, $\theta_M$, between $-0.01$ and $0.01$ at 90% confidence level, for most models. The direct search for the $Z'$ performed by the CDF Collaboration [5] excludes $Z'$ masses less than 320 GeV at 95% confidence level, for a restricted range of models.

In this paper we study the reaction

$$e^+e^- \rightarrow \gamma, Z, Z' \rightarrow f\bar{f}(\gamma),$$

(1)

where $f$ and $\bar{f}$ denote a fermion--antifermion pair, and extract the allowed range for parameters of an additional heavy gauge boson $Z'$ from the cross section and asymmetry data. For this search we use a total luminosity of 17.2 pb$^{-1}$ (corresponding to roughly 40 000 leptonic and 423 000 hadronic events) collected with the L3 detector in 1990 and 1991.

2. The L3 detector

The L3 detector at LEP covers 99% of the full solid angle. It is designed to measure energy and position of leptons and photons with high precision. A detailed description of the detector and its performance can be found elsewhere [6].

The detector consists of a time expansion chamber for the tracking and vertex reconstruction of charged particles, a high resolution electromagnetic calorimeter of 11 000 bismuth germanium oxide (BGO) crystals, a hadron calorimeter with uranium absorber and brass proportional wire chambers and a high precision muon spectrometer, consisting of three layers of multi-wire drift chambers, which measures the muon trajectory 56 times in the bending plane and 8 times in the non-bending direction. A cylindrical array of 30 scintillation counters is installed in the barrel region between the electromagnetic and the hadronic calorimeters. The luminosity of LEP is measured by the luminosity monitor, two electromagnetic calorimeters and two sets of proportional wire chambers, situated symmetrically on either side of the interaction point. Each calorimeter is a finely segmented and azimuthally symmetric array of 304 BGO crystals covering the polar angular range 24.93 $< \theta < 69.94$ mrad. All detectors are inside a 12 m inner diameter solenoid which provides a uniform magnetic field of 0.5 T along the beam direction.

3. Z lineshape measurements

Operating the LEP storage ring in the vicinity of the $Z$ mass with high luminosity permits a detailed study of the lineshape of the $Z$ resonance. We have performed measurements of the reactions

(1) $e^+e^- \rightarrow \text{hadrons},$

(2) $e^+e^- \rightarrow \mu^+\mu^-(\gamma),$

(3) $e^+e^- \rightarrow \tau^+\tau^-(\gamma),$

(4) $e^+e^- \rightarrow e^+e^-(\gamma).$

The analysis methods used for these reactions are described elsewhere [1,7]. In tables 1 and 2 we summarize the cross sections and asymmetries determined with the data. These measurements are used for our search for a $Z'$. Additionally, we include our measurements of the $\tau$ polarization [8] and the forward-backward asymmetry of the $b\bar{b}$ and $c\bar{c}$ final states [9] at $\sqrt{s} = 91.222$ GeV:

1 Deceased.
2 Supported by the German Bundesministerium für Forschung und Technologie.
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Table 1
Results on the cross sections of leptonic and hadronic final states. $\sigma$ is the cross section extrapolated to the full solid angle. In case of $e^+e^-$ final states, $t$ channel and interference contributions have been subtracted. The quoted errors exclude the luminosity uncertainty of 0.6%.

| Year | $\sqrt{s}$ (GeV) | $\sigma$ (nb) |
|------|------------------|--------------|
|      |                  | $e^+e^-\rightarrow e^+e^-$ | $e^+e^-\rightarrow \mu^+\mu^-$ | $e^+e^-\rightarrow \tau^+\tau^-$ | $e^+e^-\rightarrow$ hadrons |
| 1990 | 88.231           | 0.188±0.053   | 0.268±0.033   | 0.228±0.037   | 4.53±0.11 |
|      | 89.236           | 0.473±0.057   | 0.387±0.038   | 0.439±0.047   | 8.50±0.14 |
|      | 90.238           | 1.034±0.082   | 0.929±0.063   | 0.920±0.077   | 18.60±0.25 |
|      | 91.230           | 1.462±0.031   | 1.476±0.028   | 1.463±0.033   | 30.38±0.12 |
|      | 92.226           | 1.135±0.071   | 1.115±0.066   | 1.095±0.078   | 21.78±0.26 |
|      | 93.228           | 0.660±0.048   | 0.505±0.040   | 0.599±0.051   | 12.36±0.16 |
|      | 94.223           | 0.348±0.037   | 0.404±0.036   | 0.427±0.043   | 8.20±0.14 |

systematic error 0.5% 0.8% 1.5% 0.3%

| Year | $\sqrt{s}$ (GeV) | $\sigma$ (nb) |
|------|------------------|--------------|
| 1991 | 91.254           | 1.437±0.023   | 1.497±0.020   | 1.505±0.025   | 30.43±0.10 |
|      | 88.480           | 0.291±0.040   | 0.235±0.021   | 0.236±0.024   | 5.17±0.09 |
|      | 89.470           | 0.528±0.044   | 0.478±0.028   | 0.531±0.035   | 10.08±0.12 |
|      | 90.228           | 0.866±0.053   | 0.866±0.039   | 0.885±0.047   | 18.12±0.18 |
|      | 91.222           | 1.484±0.030   | 1.381±0.026   | 1.447±0.032   | 30.26±0.13 |
|      | 91.967           | 1.239±0.054   | 1.165±0.048   | 1.224±0.059   | 24.51±0.24 |
|      | 92.966           | 0.701±0.040   | 0.686±0.036   | 0.641±0.041   | 14.36±0.16 |
|      | 93.716           | 0.486±0.032   | 0.478±0.028   | 0.535±0.036   | 10.02±0.13 |

systematic error 0.5% 0.5% 0.7% 0.2%

$- \tau_{pol} = -0.132 \pm 0.026 \pm 0.021$,

$- A_{FB}^{\bar{b}b} = 0.086 \pm 0.015 \pm 0.007$,

$- A_{FB}^{\bar{c}c} = 0.083 \pm 0.038 \pm 0.027$.

4. Z' models

We concentrate our search for the Z' on two kinds of models which lead to an extension of the Standard Model gauge group and allow a "light" Z' with a mass between 100 GeV and 10 TeV:

- A symmetry breaking of the superstring-inspired $E_6$ gauge group [10] defines the general case of two additional neutral gauge bosons. We assume that only one of them, $Z'^0$, is light enough to be detected:

$$Z' = Z'_c \cos \Theta_6 + Z'_\psi \sin \Theta_6. \tag{2}$$

$Z'_c$ and $Z'_\psi$ are eigenstates associated with the symmetry breaking scheme of the model [10]. The parameter $\Theta_6$ determines the couplings of the heavy boson to fermions and the cases $\Theta_6 = 0, \pi/2$ and $\arctan \sqrt{3/2} - \pi$ define the $\chi$, $\psi$ and $\eta$ models. Usually, $-\pi/2 \leq \Theta_6 < \pi/2$.

- Left-right symmetric models [11] propose a right-handed SU(2)$_R$ extension of the Standard Model gauge group. The mixing between $W'_L$ and $W'_R$ is neglected and the right-handed neutrinos are assumed to be heavy. The parameter $\alpha_{LR}$ is used to describe the couplings of the heavy boson to fermions:

$$\alpha_{LR} = \sqrt{\frac{\cos^2 \theta_w - \sin^2 \theta_w}{\sin^2 \theta_w} g_L \over g_R}, \tag{3}$$

where $g_{LR}$ are the SU(2)$_{LR}$ coupling constants and $\sin^2 \theta_w$ is the weak mixing angle. If $\alpha_{LR}$ is at its lower bound, $\sqrt{2/3}$, the left-right symmetric model is identical to the $\chi$ model of the $E_6$ group. If $\alpha_{LR}$ is at its upper bound, $\sqrt{2/3}$, it corresponds to $g_L \approx g_R$. In the following, we call this special case the LR model.

The mass eigenstates, $Z$ and $Z'$, are mixtures of the symmetry eigenstates $Z^0$ of the SU(2)$_x$U(1) group and $Z'^0$ of the additional U(1) or SU(2)$_R$ groups.
Table 2
Results on forward–backward asymmetries of leptonic final states. In case of $e^+e^-$ final states, $A_{FB}$ is for the s-channel contribution only and extrapolated to the full solid angle. In case of $\mu^+\mu^-$ final states the asymmetries quoted are for acollinearity $\zeta < 15^\circ$ and in $\tau^+\tau^-$ final states for $\zeta < 14.3^\circ$.

| Year | $\sqrt{s}$ (GeV) | $A_{FB}$ ($e^+e^-\rightarrow e^+e^-$) | $A_{FB}$ ($e^+e^-\rightarrow \mu^+\mu^-$) | $A_{FB}$ ($e^+e^-\rightarrow \tau^+\tau^-$) |
|------|-----------------|--------------------------------------|------------------------------------------|------------------------------------------|
| 1990 | 88.231          | -0.034 ± 0.276                      | -0.39 ± 0.12                             | -0.42 ± 0.20                             |
|      | 89.236          | -0.205 ± 0.161                      | -0.04 ± 0.11                             | -0.09 ± 0.15                             |
|      | 90.238          | -0.111 ± 0.107                      | -0.184 ± 0.074                           | -0.18 ± 0.11                             |
|      | 91.230          | -0.023 ± 0.028                      | 0.006 ± 0.021                            | 0.07 ± 0.03                              |
|      | 92.226          | 0.042 ± 0.085                       | 0.110 ± 0.066                            | -0.04 ± 0.10                             |
|      | 93.228          | 0.053 ± 0.094                       | 0.095 ± 0.091                            | 0.11 ± 0.12                              |
|      | 94.223          | 0.129 ± 0.148                       | 0.134 ± 0.099                            | 0.02 ± 0.13                              |
|      | systematic error| 0.005                                | 0.005                                    | 0.01                                     |

| 1991 | 91.254          | 0.001 ± 0.020                       | 0.018 ± 0.015                            | 0.037 ± 0.021                            |
|      | 88.480          | -0.013 ± 0.157                      | -0.150 ± 0.100                           | -0.110 ± 0.130                           |
|      | 89.470          | -0.126 ± 0.099                      | -0.200 ± 0.070                           | -0.152 ± 0.083                           |
|      | 90.228          | -0.100 ± 0.075                      | -0.041 ± 0.052                           | -0.137 ± 0.070                           |
|      | 91.222          | 0.019 ± 0.027                       | 0.013 ± 0.021                            | -0.032 ± 0.029                           |
|      | 91.967          | 0.103 ± 0.055                       | 0.060 ± 0.045                            | 0.042 ± 0.063                            |
|      | 92.966          | 0.098 ± 0.072                       | 0.122 ± 0.058                            | 0.161 ± 0.079                            |
|      | 93.716          | 0.165 ± 0.085                       | 0.084 ± 0.067                            | 0.058 ± 0.082                            |
|      | systematic error| 0.005                                | 0.005                                    | 0.006                                    |

The mixing is described by a matrix using the mixing angle $\theta_M$:

$$\begin{pmatrix}
Z \\
Z' 
\end{pmatrix} \begin{pmatrix} 
\cos \theta_M & \sin \theta_M \\
-\sin \theta_M & \cos \theta_M
\end{pmatrix} \begin{pmatrix} 
Z_0' 
\end{pmatrix}.$$ (4)

The gauge boson masses $m_Z, m_{Z'}$ are related by the $Z$–$Z'$ mixing angle $\theta_M$:

$$\tan^2 \theta_M = \frac{m_0^2 - m_{Z'}^2}{m_{Z'}^2 - m_0^2},$$ (5)

$$m_0 = \frac{m_W}{\rho \cos \theta_w}. $$ (6)

In the absence of mixing, $m_0$ is the mass of the standard $Z$ boson. In general, $\rho$ is a free parameter. Here we investigate the case $\rho = 1$, i.e., a Higgs sector restricted to doublets.

As an example, fig. 1 shows contributions of the $\gamma$, $Z$ and $Z'$ exchange and their interference for $m_{Z'} = 500$ GeV and $\theta_M = 0.1$ in the $\chi$ model. We see that even for $Z'$ masses far outside the LEP energy range, $Z$–$Z'$ mixing modifies the shape of the $Z$ resonance. Propagator effects of the $Z'$ itself cannot be detected.

Fig. 1. Born level contributions to $\sigma(e^+e^-\rightarrow \mu^+\mu^-)$ of the $ZZ, \gamma Z$ terms in the Standard Model and the $ZZ, \gamma Z$ and $\gamma Z' + ZZ' + Z'Z'$ terms of an assumed $Z'$ in the $\chi$ model with $m_{Z'} = 500$ GeV and $\theta_M = 0.1$. 192
if the mass is high. Therefore, the searches for the Z' at LEP are mainly sensitive to the mixing angle, but not to the Z' mass.

5. Z, Z' lineshape analysis

The determination of limits on $\theta_M$ and $m_{Z'}$ in the framework of the above models necessitates a program for the calculation of cross sections and asymmetries that includes all relevant radiative corrections. To allow a comparison and cross check with an analysis without a Z', we used the program ZEFIT version 3.1 [12] together with the program ZFITTER version 4.5 [13]. ZEFIT is a complement to ZFITTER which contains the modifications to the Z lineshape due to a high mass Z'. Initial and final state QED corrections are considered to $O(\alpha^2)$, higher order corrections for initial state radiation are considered with common photon exponentiation. Weak loop corrections for the Z boson are included to $O(\alpha)$ and are supplemented with the $O(\alpha, \alpha_s)$ and the leading $O(\alpha^2 m_t^4/m_W^4)$ corrections from the top quark insertions in the gauge boson self-energies. Weak loop corrections for the Z' are neglected.

The data listed in tables 1 and 2 have systematic uncertainties in addition to their statistical errors. We consider a partial error correlation when calculating $\chi^2$,

$$\chi^2 = D^T V^{-1} D,$$  

where $D$ is a column vector with elements such as $(\sigma^{th} - \sigma^{exp})$ and $(A^{th} - A^{exp})$ and $V$ is the $N \times N$ error correlation matrix between measurements. The diagonal elements of $V$ are given by the quadratic sum of the statistical and systematic errors, while the off diagonal elements are given by the product of the common systematic errors. This is generalized to the common systematic error between different data sets. The procedure to implement the LEP energy uncertainty is described in detail elsewhere [14].

6. Results

6.1. Shift of the Z mass

When we include the effects of a possible Z' in a fit to our measurements, the Z mass shifts with respect to the one determined in the Standard Model framework. We fit the mixing angle $\theta_M$ and the standard Z mass, $m_Z$, for different assumed masses $m_{Z'}$. The mass difference

$$\Delta m = m_Z(Z, Z') - m_Z(SM),$$  

where $m_Z(Z, Z')$ is the result of a fit including Z, Z' and mixing, while $m_Z(SM)$ denotes the result of a Standard Model fit, is shown in fig. 2 as a function of $m_{Z'}$ for the $\chi$, $\psi$, $\eta$ and LR models. We used our measured value $m_Z(SM) = (91.195 \pm 0.009)$ GeV [1]. The shift $\Delta m$ deviates from zero by less than one standard deviation. The increase of $m_Z$ for $m_{Z'} < 500$ GeV is due to both Z-Z' mixing and Z' exchange effects. Above $m_{Z'} = 500$ GeV, $m_Z$ is decreased by Z-Z' mixing since the Z' exchange is negligible. The correlations between $\theta_M$ and $m_Z$ or $m_{Z'}$ and $m_Z$, respectively, are negligible.

![Fig. 2. Difference between the Z mass determined from a Standard Model fit and the mass determined including a potential Z' as well as mixing.](image-url)
Fig. 3. The 95% CL allowed regions in the $m_{Z'}$ versus $\theta_M$ plane in (a) the $\chi$ model, (b) the $\psi$ model, (c) the $\eta$ model and (d) the LR model. The Higgs mass is fixed to $m_H = 300$ GeV. The dashed lines correspond to $m_t = 100$ GeV, the solid lines to $m_t = 150$ GeV and the dash-dotted lines to $m_t = 200$ GeV.

6.2. Limits on $\theta_M$ and $m_{Z'}$

In general, the models we consider depend on the following free parameters: $m_\beta$, $m_{Z'}$, $\theta_M$, $m_t$, $m_H$, $\alpha_s$ and $Z'$ model parameters such as $\Theta_k$ or $\alpha_{LR}$. In order to reduce the number of free parameters we fix the Higgs mass, $m_H = 100$, 300 and 1000 GeV, the top mass, $m_t = 100$, 150 and 200 GeV and $\alpha_s = 0.12$. The $Z$ mass is limited to the range $m_Z = (91.195 \pm 0.009)$ GeV. Thus, the free parameters are $\theta_M$, $m_{Z'}$, and $\Theta_k$ or $\alpha_{LR}$. First, we compare the cross sections and asymmetries with the predictions of the special $E_6$ models $\chi$, $\psi$ and $\eta$ as well as the LR model. In order to determine the allowed regions for the parameters $\theta_M$ and $m_{Z'}$ within a particular model we require $\chi^2 \leq \chi^2_{\text{min}} + 5.99$, corresponding to the 95% confidence limits for two parameters. The results are shown for the $\chi$, $\psi$, $\eta$ and LR model in fig. 3. We find only weak dependences of the contours on the top mass.

Fig. 4 shows the 95% CL allowed range of the $Z$–$Z'$ mixing angle for the whole range of $\Theta_k$ and $\alpha_{LR}$, for the two cases $m_{Z'} > 200$ GeV and $> 700$ GeV. The top mass and Higgs mass are set to 150 GeV and 300 GeV, respectively. In fig. 5 we compare limits on $\theta_M$ and $m_{Z'}$ obtained in the $\chi$ model for different values of the Higgs mass ($m_H = 100$, 300 and 1000 GeV).
Our search for a $Z'$ is mainly sensitive to the $Z-Z'$ mixing angle, $\theta_M$. There are no indications for the existence of a $Z'$; the fitted $Z-Z'$ mixing angle is compatible with zero for all models considered. Allowed values for the mixing angle are typically between $-0.010$ and $0.015$ at the 95% CL. The influence of the top mass and the Higgs mass on these limits is small. These limits from L3 data substantially improve the existing limits for $\theta_M$ [4].

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