Attenuation of super-soft X-ray sources by circumstellar material

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ABSTRACT
Recent studies have suggested the possibility of significantly obscuring super-soft X-ray sources in relatively modest amounts of local matter lost from the binaries themselves. If correct, then this would have explained the paucity of observed super-soft X-ray sources and would have significance for the search for single-degenerate type Ia supernova progenitors. We point out that earlier studies of circumbinary obscuration ignored photo-ionisations of the gas by the emission from the super-soft X-ray source. We revisit the problem using a full, self-consistent calculation of the ionisation state of the circumbinary material photo-ionised by the radiation of the central source. Our results show that the circumstellar mass-loss rates required for obscuration of super-soft X-ray sources is about an order of magnitude larger than those reported in earlier studies, for comparable model parameters. While this does not entirely rule out the possibility of circumstellar material obscuring super-soft X-ray sources, it makes it unlikely that this effect alone can account for the majority of the missing super-soft X-ray sources. We discuss the observational appearance of hypothetical obscured nuclear burning white dwarfs and show that they have signatures making them distinct from photo-ionised nebulae around super-soft X-ray sources imbedded in the low density ISM.

Key words: binaries: close – supernovae: general – white dwarfs – X-rays: binaries – radiative transfer – circumstellar matter – winds, outflows

1 INTRODUCTION
The topic of a massive white dwarf accreting hydrogen-rich material from a non-degenerate companion and processing that material into heavier elements on its surface is of relevance to the understanding of a number of astrophysical objects, including symbiotics (e.g. Minkowicska 2012) and single-degenerate type Ia supernova progenitors (e.g. Maoz et al. 2014). In the the case of the single-degenerate scenario, the accretion process is necessary for the white dwarf to grow in mass until it becomes massive enough to undergo thermonuclear runaway in its degenerate core and explode. The steady burning of accreted hydrogen-rich material on the surface of a massive white dwarf is believed to be possible only in a narrow interval of mass-accretion rates (Nomoto 1982; Shen & Bildsten 2007), and the process is expected to emit copious amounts of super-soft X-rays (van den Heuvel et al. 1992; Kahabka & van den Heuvel 1997). However, several studies have established a discrepancy of one to two orders of magnitude between the expected and observed number of systems, as well as the integrated luminosities of super-soft X-ray sources in old galactic populations, provided type Ia supernova progenitors are in fact single-degenerates (Gilfanov & Bogdán 2010; Di Stefano 2010).

The missing super-soft X-ray sources could perhaps be explained if the X-ray emitting systems were obscured by local material. There is growing evidence for the presence of circumstellar material around at least a subset of type Ia supernova progenitors as inferred from supernova spectra (Gerardy et al. 2004; Patat et al. 2007; Simon et al. 2008; Sternberg et al. 2011; Cao et al. 2015), as well as from historical supernova remnants (Borkowski et al. 2006; Chiotellis et al. 2012; Broersen et al. 2014).

Circumstellar material around type Ia supernova progenitors could be supplied in a variety of ways, e.g. by a wind from either of the binary components, stellar pulsations of the companion, incomplete accretion of wind-Roche lobe overflow (Mohamed & Podsiadlowski 2007), or tidal interactions between the components (Chen et al. 2011). The effect of circumstellar obscuration on the observability of super-soft X-ray emission from progenitor systems was investi-
gated by Nielsen et al. (2013); Wheeler & Pooley (2013). Both studies suggested that relatively modest amounts of circumstellar material could obscure super-soft X-ray sources to the point where they would no longer be detectable with current X-ray telescopes. However, both studies either ignored or used rather simple assumptions concerning the effect of photo-ionisation of the circumstellar material, and specifically did not take photo-ionisations of metals into account. The present study seeks to remedy those shortcomings by conducting a full treatment of the photo-ionisation of the obscuring circumstellar material, to get a more accurate handle on how much circumstellar material is required for obscuration.

The reader should note the terminology used in the following: mass-transfer rate denotes the rate of mass transferred from the donor to the accretor, regardless of whether the transferred material is retained on the accretor; just accretion rate – or just mass-accretion rate – is the rate of mass lost from the binary into the circumbinary region in which it may obscure the super-soft X-ray source. We use the symbol \( M_w \) for the latter.

In Section 2 we describe our model, Section 3 presents the results of our calculations, while Section 4 discusses the implications of the results. Section 5 concludes.

## 2 MODEL

The geometry of the model examined in this study is identical to the one considered in Nielsen et al. (2013). The primary difference between that study and the present one is the incorporation of full photo-ionisation calculations. In particular, we consider a super-soft X-ray source inside a spherically symmetric shell of material, surrounded by vacuum. Throughout the following, we assume that the source is a blackbody, with effective temperature \( kT_{\text{eff}} \) between 30 eV and 150 eV, and luminosities \( L_{\text{bol}} \) between 10\(^{37}\) erg/s and 10\(^{38}\) erg/s, parameters characteristic of ‘canonical’, persistent super-soft X-ray sources (van den Heuvel et al. 1992; Kahabka & van den Heuvel 1997).

The gas shell surrounding the source is defined by an inner and outer boundary \((r_{\text{inn}} \text{ and } r_{\text{out}}\text{, respectively})\), and the density is given by an \( r^{-2} \)-law, characteristic of spherically symmetric, constant-velocity wind mass loss:

\[
\rho(r) = \frac{M_w}{4\pi u_w} \left( \frac{1}{r_{\text{inn}}} - \frac{1}{r_{\text{out}}} \right)
\]

where \( \rho(r) \) is the mass density as a function of radius, \( M_w \) is the mass-loss rate into the circumstellar region and \( u_w \) is the velocity of the wind, assumed to be constant in the region of interest. Inside the inner and outside the outer boundaries we assume vacuum. The inner radius can be envisioned as equivalent to the orbital radius of the binary (see also Sections 3 & 4.2). Realistic density profiles are likely to be more complex than this, and clearly depend on the mass-loss history of the binary, however, the simple \( r^{-2} \) profile is a useful first approximation and also facilitates comparison with previous results.

### 2.1 Order-of-magnitude estimates

The total mass of the gas shell is

\[
M_w = \frac{M_w}{u_w} \left( u_{100} - u_{100} \right)
\]

\[
= 9.5 \times 10^{25} \left( 1 - \frac{u_{100}}{u_{100}} \right) M_{\odot} u_{100} r_{\text{out,AU}} g
\]

where \( M_{w,10} \) is the mass loss rate in units of 10\(^{-6}\) M\(_{\odot}\)yr\(^{-1}\), \( u_{100} \) is the outflow velocity in units of 100 km/s and \( r_{\text{out,AU}} \) is the outer radius of the shell in astronomical units.

The column density of the gas shell is:

\[
N_{\text{H}} = \frac{M_w}{4\pi u_w m_p u_{100} \left( 1 - \frac{r_{\text{out}}}{r_{\text{inn}}} \right)}
\]

\[
= 1.4 \times 10^{22} \left( 1 - \frac{r_{\text{inn}}}{r_{\text{out}}} \right) M_{w,10}^2 u_{100}^{-1} r_{\text{out,AU}}^{-1} \text{cm}^{-2}
\]

where \( \mu \approx 1.4 \) for Solar abundance, and \( m_p \) is the mass of the proton. A column density of \( \approx 10^{22} \text{cm}^{-2} \) of neutral material of Solar abundance can easily obscure emission from a super-soft source with temperature of \( \approx 100 \text{eV} \), as discussed in Nielsen et al. (2013); Wheeler & Pooley (2013). However, photo-ionisation of the wind material by the emission from the super-soft source can significantly reduce its opacity.

Similar to the classical Strömgren sphere problem, the effect of the photo-ionisation can be estimated, to the first approximation, by comparing the total rates of photo-ionisation and recombination in the gas shell:

\[
N_w = \int \frac{h \nu}{\nu} L_{w} d\nu = f \frac{L}{h \nu_0}
\]

\[
= \int n^2 \alpha_{\text{rec}} d^3r = \frac{M_w^2}{4\pi u_w^2 m_p^2 n_{100}^2} \left( \frac{1}{r_{\text{inn}}} - \frac{1}{r_{\text{out}}} \right)
\]

where \( h \nu_0 \) is the photo-ionisation threshold of the main absorbing ion, \( \alpha_{\text{rec}} \) its recombination coefficient, \( L \) is the luminosity of the central source and the factor \( f \) depends on its radiation spectrum. In Eq. 6, it was assumed that the gas shell is optically thick to the radiation of the central source (in the absence of photo-ionisation). If the photo-ionisation rate \( N_w \) exceeds the recombination rate \( N_r \), the shell material will be fully ionised and therefore transparent to the radiation of the central source. The critical value of the mass outflow rate is determined by the condition \( N_w = N_r \). At lower \( M_w \) the gas shell is fully ionised and transparent, whereas at higher outflow rates it is opaque to the radiation of the central source. For monoatomic hydrogen gas, the value of the critical outflow rate can be computed straightforwardly; with \( h \nu_0 = 13.6 \text{eV} \) and \( \alpha_{\text{rec}} = 2.6 \times 10^{-13} \text{cm}^2\text{sec}^{-1} \) (case B) one obtains:

\[
M_{w,\text{crit}} = 2.2 \times 10^{-5} (f L_{38})^{1/2} u_{100}^{1/2} r_{\text{out,AU}}^{-1/2}
\]

\[
\times \left( 1 - \frac{r_{\text{inn}}}{r_{\text{out}}} \right)^{-1/2} M_{\odot} / \text{yr}
\]

where \( L_{38} \) is the luminosity in units of 10\(^{38}\) erg/s. For the central source temperature of \( kT_{\text{eff}} = 100 \text{eV} \), for example, \( f \approx 5 \times 10^{-2} \) and the leading factor in Eq. 6 becomes \( 4.9 \times 10^{-6} M_{\odot} \text{yr}^{-1} \). Eq. 6 is sufficiently accurate for hydrogen gas shell, but gives only an order of magnitude estimate for gas of solar abundance. The latter case requires a more careful account of the ionisation state of the main absorbing species. However, Eq. 6 predicts a nearly correct
scaling of the critical mass loss rate (as confirmed by Cloudy calculations in the following sections):

$$M_{w,\text{crit}} \propto L^{1/2} u_w r_{\text{inn}}^{1/2} \left(1 - \frac{r_{\text{inn}}}{r_{\text{out}}}\right)^{-1/2}$$

(7)

As one can see from Eq. (7), the critical mass loss rate relatively weakly depends on the luminosity of the central source and the inner radius of the shell and is nearly insensitive to the outer radius of the shell (for sufficiently large \(r_{\text{out}}/r_{\text{inn}}\)). The latter should be expected, given the steepness of the assumed density profile.

The above considerations strictly apply to a stationary gas shell. In the case of the wind, (presumably) neutral material is continuously added at the inner edge of the shell. It is promptly\(^1\) photo-ionised by the radiation from the central source. However, if the new material is added at a sufficiently large rate – i.e. one comparable to the photon injection rate – it will screen the rest of the shell from the ionising radiation, thus reducing its degree of ionisation and increasing its opacity. The importance of advection is determined by the ratio of the rate at which new material is added to the inner edge of the shell to the injection rate of ionising photons:

$$\frac{\dot{N}_{\text{gas}}}{\dot{N}_{\text{phot}}} = 6 \times 10^{-5} M_{w,-6} (f_{-1} L_{38})^{-1}$$

(8)

where \(f_{-1}\) is the factor \(f\) in units of \(10^{-1}\). The ratio given in Eq. (8) becomes of the order of unity at \(M_w \sim 10^{-2} M_\odot \text{yr}^{-1}\), which is much larger than the mass outflow rates considered here.

2.2 Cloudy calculations

For detailed photo-ionisation calculations, we used the one-dimensional photo-ionisation code Cloudy, version 13.02 (for a detailed description of the latest release of Cloudy see Ferland et al 2013). Cloudy calculates the ionisation and thermal state of a cloud of gas that is irradiated by a central source, by simultaneously solving equations of photo-ionisation and thermal equilibrium. It is assumed that atomic processes in the gas have become time-steady. This assumption is reasonable, at least in the context of single-degenerate type Ia supernova progenitors, since all microphysical time scales in the shell are much shorter than time scales relevant to super-soft sources. In our simulations, we fix the density distribution and compute the gas temperature self-consistently, as maintained by the photo-ionisation of the gas by the central source. For the gas density distribution, we use the built-in dilaw wind option in Cloudy which reproduces the density structure in Eq. (1), and the sphere keyword as appropriate for a closed geometry. The advection effects are not included in our calculations, as justified above. Cloudy’s output files specify the emergent spectrum, temperature, pressure, and ionisation structure, in addition to a host of other data.

We run Cloudy for three values of \(u_w\): 10, 50, 100 km/s. This spans the likely wind velocities expected from red giant and asymptotic giant star donors (Owocki 2013). For the purposes of this study we do not specify the nature of the wind. For each combination of \(L_{\text{bol}}, kT_{\text{eff}}, r_{\text{inn}}, r_{\text{out}}\) and \(u_w\) we run Cloudy for a range of values of \(M_w\) from \(10^{-10} M_\odot \text{yr}^{-1}\) to \(10^{-5} M_\odot \text{yr}^{-1}\).

The chemical composition of the material in the shell is Solar, as given in Grevesse et al. (2010). In Subsection 3.3 we compare this with the abundances used in Nielsen et al. (2013).

For hydrogen and helium, Cloudy can be expected to give reliable results up to \(n \sim 10^{19} \text{ cm}^{-3}\). However, for number densities \(\gg 10^{10} \text{ cm}^{-3}\) the full treatment of a plasma containing heavier elements should not be considered reliable, see the Cloudy manual ‘Hazy’2. For comparison, the largest value of \(M_w\) for which one of our plots have data points \((10^{-5} M_\odot / \text{yr} \times r_{\text{inn}} = 1 \text{ AU} \text{ and } u_w = 50 \text{ km/s} \text{ on Figure 5})\) corresponds to the number density of \(1.9 \times 10^{10} \text{ cm}^{-3}\), i.e. within the nominal density range of Cloudy.

3 RESULTS

Cloudy’s output can be used to reconstruct the spectrum of the system consisting of the super-soft X-ray source and circumstellar cloud, along with the ionisation structure of the circumstellar material. In the following, we use the term output spectrum to mean the sum of the spectrum of transmitted radiation and the emission from the irradiated cloud. For the output data, we concentrate on the photon energy interval between 0.3 and 1.5 keV. Below 0.3 keV, even a modest ISM column effectively blocks any super-soft emission, and above 1.5 keV the emitted energy of a super-soft X-ray source is negligible.

To quantify how the attenuation depends on the various input parameters, we calculated the integrated emitted super-soft luminosity \(L\) of the output spectrum for each input configuration and compared this with the integrated emitted luminosity of the unabsorbed super-soft source spectrum, \(L_0\) (using the photon energy interval between 0.3 and 1.5 keV as integration limits). This yielded a transmission ratio \(L/L_0\) between 1 (no obscuration) and 0 (complete obscuration) for each input configuration.

3.1 Attenuation of super-soft emission

To demonstrate the general trends in our results, Figure 3 shows a comparison between the unabsorbed input spectrum of a \(kT_{\text{eff}} = 50 \text{ eV}, L_{\text{bol}} = 10^{38} \text{ erg/s blackbody source}, \text{and the output spectra in a cloud with inner and outer radii of 1 and 10 AU, respectively, and } u_w = 50 \text{ km/s, for three values of } M_w \text{ from } 1 \times 10^{-7} M_\odot \text{yr}^{-1} \text{ to } 1 \times 10^{-6} M_\odot \text{yr}^{-1}.\text{For the smallest mass-loss rate shown the output spectrum is only weakly attenuated. For larger values of } M_w, \text{ absorption edges of various neutral and ionised species appear in the spectrum along with their line and recombination emission. Among the absorption edges, the most significant is OVII around } \sim 739 \text{ eV. At } M = 1 \times 10^{-6} M_\odot \text{yr}^{-1} \text{ the } 0.3-1.5 \text{ keV flux is attenuated by a factor of } \approx 0.30.\text{The behaviour shown in Figure 3 is qualitatively similar}

\(^1\) the photo-ionisation time at the inner edge of the gas shell is of the order \(\tau_{\text{ph}} \sim 10^{-3} - 10^{-2} \text{ s.}\)

\(^2\) Sect.3.8 on p.35 in ‘Hazy’ Part 2 for Cloudy c13.1. The two Hazy manuals are downloadable with the Cloudy installation files on [http://nablado.org/wiki/DownloadLinks](http://nablado.org/wiki/DownloadLinks)
for other configurations of $kT_{\text{eff}}$, $r_{\text{inn}}$, $r_{\text{out}}$, and $u_w$, although the critical mass-loss rate where obscuration becomes significant is of course different for different combinations of parameters. Results of our calculations are summarised in Figure 2, where we show the attenuation curves as a function of the mass loss rate for different values of the source temperature and gas shell parameters. Table 1 gives the $\dot{M}_{\text{w, crit}}$ values required to produce an attenuation of a factor of $10^2$. It also lists the corresponding column densities of the gas shell $N_H$.

### 3.2 Parameter dependence

Figure 3 shows comparisons between attenuation curves for different combinations of inner and outer radii, as a function of the circumstellar mass loss rate. In agreement with the scaling suggested by Eq. (7), the attenuation curve is moderately dependent on the value of the inner radius and nearly insensitive to the position of the outer boundary of the shell, as long as $r_{\text{out}}/r_{\text{inn}}$ is sufficiently large.

Dependence of the attenuation curve on the luminosity of the central source is illustrated in Figure 4. As one can see from the plot, it is somewhat weaker than predicted by Eq. (7). This is because the derivation of Eq. (7) did not take collisional ionisation into account.

As the gas density in the shell is determined by the ratio $\dot{M}_w/u_w$, the attenuation curves shift along the $\dot{M}_w$ axis linearly with the outflow velocity. This is obvious from Figure 2 and Table 1 (cf. Eq. (7)).

### 3.3 Chemical abundances

The chemical abundances used in Nielsen et al. (2013) were taken from Anders & Ebihara (1982) (for all other elements than helium) and Peimbert & Torres-Peimbert (1977) (for helium), as tabulated in Morrison & McCammon (1983). The present study used the more updated chemical abundances table from Grevesse et al. (2010). Figure 5 shows a comparison between the attenuation curves for the two abundance tables, when calculated with Cloudy using otherwise identical input parameters. For reference, the 'GASS10' curve in Figure 5 is the same as the '1.0-10 AU' curve in the second panel from the top, middle column on Figure 2. As Figure 5 shows, the difference between the transmission curves computed for the two abundance tables is insignificant. For comparison, a transmission ratio of $10^{-1}$ corre-
L/L

L/L

L/L

L/L

L/L

L/L

4 DISCUSSION

The results presented above demonstrate the importance of the proper account for photo-ionisation when considering attenuation of super-soft X-ray sources by circumbinary material. In particular, the values of $\dot{M}_w$ required for significant obscuration of a canonical super-soft X-ray source are about an order of magnitude larger than those reported in Nielsen et al. (2013). Figure shows a direct comparison be-

Figure 2. Attenuation of a super-soft source as a function of the mass outflow rate $\dot{M}_w$. The super-soft radiation is assumed to have a blackbody spectrum with luminosity of $L_{bol} = 10^{38} \text{ erg/s}$, and the luminosity emerging from the system is integrated from 300 eV to 1500 eV. The three columns of panels show results for different outflow velocities: $u_w = 10 \text{ km/s}$ (left) $u_w = 50 \text{ km/s}$ (middle) and $u_w = 100 \text{ km/s}$ (right). Different panels in each column correspond to different values of the source temperature (marked in the upper-right corners of each panel) and different curves in each panel correspond to different values of the inner radius of the gas shell, as marked in the plots. The outer boundary of the shell is $r_{out} = 10 \text{ AU}$ in all cases.

Figure 4. Attenuation curves for different values of the luminosity of the central source. Other parameters are fixed at the following values: $KT_{\text{eff}} = 50 \text{ eV}$, $u_w = 50 \text{ km/s}$.

Figure 5. Comparison between attenuation curves computed for the abundance table of (Grevesse et al. 2011) (marked GASS10) and the older one used in Nielsen et al. (2013) (marked MM83), for $KT_{\text{eff}} = 50 \text{ eV}$, $L_{bol} = 10^{38} \text{ erg/s}$, $r_{inn} = 1 \text{ AU}$, $r_{out} = 10 \text{ AU}$ and $u_w = 50 \text{ km/s}$.

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The results presented above demonstrate the importance of the proper account for photo-ionisation when considering attenuation of super-soft X-ray sources by circumbinary material. In particular, the values of $\dot{M}_w$ required for significant obscuration of a canonical super-soft X-ray source are about an order of magnitude larger than those reported in Nielsen et al. (2013). Figure shows a direct comparison be-
for the same input values of parameters, that this amount of obscuration would require a mass loss into the circumstellar region of \( \gtrsim 50\% \) of the mass-transfer rate, i.e. the amount of material lost into the circumstellar region would have to be of the order as the material being accreted onto the white dwarf. For wind velocities of \( \sim 50 - 100 \) km/s the circumstellar mass loss rate should exceed \( \gtrsim 90\% \) of the mass-transfer rate, i.e. \( \sim 10 \) times more material should be lost into the circumstellar space than be accreted on to the white dwarf. Recalling that the steady-burning rate for a massive white dwarf is a few times \( 10^{-7} M\odot\text{yr}^{-1} \), this means that to sustain both the steady burning super-soft X-ray source and the obscuring envelope the donor would have to lose \( \gtrsim 10^{-6} M\odot\text{yr}^{-1} \) for a \( \gtrsim 10^8 \) years. The high mass-loss rate and the total mass lost (around a Solar mass or more) constrains the population of possible donors, and hence binary systems capable of producing significantly obscured, super-soft X-ray sources that eventually reach the Chandrasekhar mass and becomes type Ia supernovae.

Although we considered here a specific case of the circumbinary wind, interpreted broadly, our results show that a canonical super-soft source is capable of ionising about \( N_H \sim 10^{22} - 10^{23} \text{cm}^{-2} \) of material located at the distance of a \( \sim \) few astronomical units from the source (Table 1).

Looking from a different perspective, a narrow but dense shell of gas with the hydrogen column density in excess of \( \sim 10^{23} \text{cm}^{-2} \) around a single-degenerate type Ia supernova progenitor could conceivably obscure the super-soft X-ray emissions from such a system. Because of the large velocities of supernova ejecta (upwards of \( \sim 10,000 \) km/s or \( \sim 5.8 \) AU/day – for type Ia supernovae) such a shell would be overtaken by the ejecta within a matter of days. Hence, upper limit measurements from e.g. radio observations would need to be made almost immediately after the supernova explosion to provide useful constraints on the amount of circumbinary material present at the \( \sim \)AU distances from the supernova. The example of nearby SN2011fe is probably to be considered a best case in this respect, as it was discovered and subjected to follow-up observations almost immediately after exploding (Nugent et al. 2011). Even so, the radio limits placed on SN2011fe were based on observations conducted a little over two days after the supernova (Chomiuk et al. 2012), which means that the blast wave

| \( u_w \) [km/s] | \( T_{\text{eff}} \) [eV] | \( r_{\text{inn}}, r_{\text{out}} \) [AU] | \( M_{w,\text{crit}} \) [M\odot yr\(^{-1}\)] | \( N_H \) [cm\(^{-2}\)] |
|--------------|----------------|----------------|----------------|---------|
| 10.0 | 30.0 | 0.1, 10 | 3.6 \times 10^{-8} | 5.2 \times 10^{22} |
| * | 0.5, 10 | 1.3 \times 10^{-7} | 3.2 \times 10^{22} |
| * | 1.0, 10 | 2.0 \times 10^{-7} | 2.6 \times 10^{22} |
| 50.0 | 0.1, 10 | 8.2 \times 10^{-8} | 1.2 \times 10^{23} |
| * | 0.5, 10 | 2.1 \times 10^{-7} | 5.8 \times 10^{22} |
| * | 1.0, 10 | 3.5 \times 10^{-7} | 4.5 \times 10^{22} |
| 100.0 | 0.1, 10 | 1.6 \times 10^{-7} | 2.3 \times 10^{23} |
| * | 0.5, 10 | 3.5 \times 10^{-7} | 9.5 \times 10^{22} |
| * | 1.0, 10 | 5.1 \times 10^{-7} | 6.6 \times 10^{22} |
| 150.0 | 0.1, 10 | 2.0 \times 10^{-7} | 2.8 \times 10^{23} |
| * | 0.5, 10 | 4.1 \times 10^{-7} | 1.7 \times 10^{23} |
| * | 1.0, 10 | 6.1 \times 10^{-7} | 7.9 \times 10^{22} |

Table 1. Values of the mass-loss rate and corresponding \( N_H \), needed for an attenuation of \( L_{\text{obs}}/L_0 = 0.01 \).
Figure 7. Broad band (infrared to X-ray) spectra of an attenuated super-soft X-ray source for three different attenuation levels: an unobscured source ($M = 10^{-9} M_\odot/yr$), moderately obscured source ($M = 5 \times 10^{-7} M_\odot/yr$) and heavily obscured source ($M = 3 \times 10^{-6} M_\odot/yr$). The model parameters are at their default values: $kT_{\text{eff}} = 50$ eV, $L_{\text{bol}} = 10^{38}$ erg/s, $r_{\text{in}}$, $r_{\text{out}} = 1$ AU, 10 AU. The dashed black line is the incident spectrum.

would have moved to a distance of $\sim 12$ AU (assuming the above-mentioned ejecta velocity) at the time observations began. Hence, a very dense shell of material of, say, between 1 and 10 AU from the exploding object may conceivably have eluded detection, as the supernova ejecta would have passed through the obscuring medium before observations began. More distant type Ia supernovae are typically discovered several days to weeks after the explosion, and in such cases radio observations should not be expected to yield upper limits capable of ruling out narrow configurations of circumstellar material. However, since single-degenerate progenitors of type Ia supernovae need to be super-soft X-ray sources for extended periods of time and require continuous mass-loss rates $\gtrsim 10^{-6}$Myr$^{-1}$ to remain hidden, the extent and mass of the circumstellar gas surrounding such sources could be much larger than the narrow configurations mentioned above and should therefore, theoretically at least, be detectable via post-supernova radio observations. Also, such extended systems should be detectable in pre-supernova observations in the recombination lines of hydrogen and helium and forbidden lines of metals (cf. Woods & Gilfanov 2013).

4.1 Observational appearance of obscured SSS

Although circumbinary obscuration is unlikely to explain the paucity of super-soft sources in the context of progenitors of type Ia supernovae, it is plausible that stably nuclear-burning white dwarfs experience various degree of circumbinary obscuration. In particular, this may be one of the factors (along with the reasons intrinsic to the population synthesis calculations) explaining the discrepancy between the number of super-soft sources predicted in population synthesis studies and their observed numbers (e.g. Chen et al. 2014, 2013). While quenching the bulk of the X-ray emission from the stably nuclear-burning white dwarf, circumbinary obscuration leads to the appearance of various emission signatures at all wavelengths (including X-ray band itself), which can be exploited to search and identify such obscured super-soft X-ray sources.

Figure 7 shows the output spectrum of an attenuated super-soft X-ray source in the broad wavelength range from infrared to X-ray wavelengths. Spectra for three values of the mass-loss rate $M_\nu$ are shown, corresponding to different obscuration levels in the X-ray band – from completely unobscured to completely obscured source (cf. Fig 2). In the completely unobscured case, the gas in the wind is nearly fully ionised and optically thin, and the attenuation at these mass-loss rates is negligible (save for a short period when the source initially ‘turns on’ and ionises the cloud). Such sources would be similar to naked super-soft sources when observed in X-rays, as discussed previously. In the obscured case, the soft X-ray radiation is reprocessed to the optical and UV bands, giving rise to copious emission lines. In the intermediate case of moderate obscuration a number of emission features can be observable in the X-ray band as well.

4.1.1 X-ray lines

X-ray lines, although not the brightest among the emission features in our calculations, can carry away up to $\sim 10^{-4} - 10^{-3}$ of the luminosity of the central source. The brightest among them are resonant lines of H-like ions and He-like triplets of the low-Z metals. In Figure 1 we show luminosities of several of the brightest X-ray lines as a function of the mass-loss rate. As the amount of the circumbinary material increases with the mass-loss rate, luminosities of these lines initially grow with $M_\nu$, until obscuration in the X-ray region sets in at $\sim 10^{-6} M_\odot/yr$ (see Figure 2). At this point, the X-ray line luminosities plummet due to absorption by the neutral outer layers of the wind. The behaviour of particular lines is mainly determined by the changes of relative abundances of respective ions, with the intrinsic line ratios being characteristic for photo-ionised plasma with ionisation parameter of $\xi \approx 37.4 L_{38} M_{-6}^4 u_{100}$. However, as the mass-loss rate approaches the critical value, the escaping line lu-

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minosities and their ratios are significantly modified by the absorption by the neutral outer part of the wind, giving rise to the patterns shown in Fig. 8.

Ness et al. (2013) studied high-resolution spectra for a number of super-soft X-ray sources in local galaxies. Based on these observations, they suggested a subdivision of super-soft X-ray sources into two classes: SSa (‘absorbed’) and SSe (‘emitting’) – the former having generally blackbody-like spectra with some prominent absorption features, and the latter showing strong emission features (comparable in strength to the continuum) superimposed on weak blackbody spectra. When correlated with the inclinations of the systems of that study (and with the caveat that inclination determination is quite problematic in most of the cases) members of the SSa class were predominantly high-inclination systems, while SSe systems were predominantly viewed more edge-on. This led Ness and collaborators to suggest that the spectral differences of the two classes might arise as a result of viewing-angle, rather than from intrinsic differences between the systems themselves, conceptually similar to the viewing-angle effect in the unified model for AGNs. Although the direct comparison with observed spectra is outside the scope of the present work, our study does recreate several of the features of the SSe class reported in Ness et al. (2013) in the interval where the central sources transition from unobscured to fully obscured regime. The two strongest emission features in the spectra of U Sco and CAL 87 on Figure 3 in Ness et al. (2013) correspond to the O VIII-doublet at 18.97Å, 18.98Å, and the line blend consisting of the N VII-doublet at 24.78Å, 24.79Å, and the N VI at 24.89Å. We find the same features are prominent in our spectra, as seen on our Figure 11. Several other, less pronounced lines in our spectra can be also found in the observed spectra of U Sco and CAL 87, e.g. Ne IX at 13.45Å, O VIII at 21.6Å, and possibly three N VI lines around 29Å (28.78Å, 29.1Å, 29.5Å). At lower X-ray energies the similarities between our spectra and those of Ness et al. (2013) become less obvious, presumably due to interstellar absorption in the observed spectra. The fact that our relatively simple model setup can reproduce some of the features of the SSe spectra discussed in Ness et al. (2013) is not in itself surprising, since any model with significant incident luminosity in X-rays which interacts with a Solar metallicity gas is likely to produce a somewhat similar set of emission features. However the luminosities of these lines, their ratios and the presence and strength of absorption lines and edges are determined by the details of the model such as geometry of the gas and emission pattern, ionisation parameter and chemical abundances. Detailed analysis of these effects is beyond the scope of the present paper.

4.1.2 Optical lines

As the mass-loss rate \( \dot{M}_\text{w} \) grows towards full obscuration, the X-ray emission is gradually quenched, and the absorbed energy increasingly re-emitted at UV and optical energies. In this regime, copious emission lines in the UV, optical and infrared bands are produced in the photo-ionised wind material. The majority of these lines (except for extreme UV lines), unlike X-ray lines, escape the wind material without significant attenuation and therefore may serve as a valuable diagnostic tool in the search for and identification absorbed super-soft sources.

Figure 8 shows the luminosity of a number of observationally relevant lines of hydrogen and helium as well as forbidden lines of metals as a function of the mass-loss rate. The luminosity of hydrogen and helium recombination lines grows monotonically with mass-loss rate and then saturate as the central source becomes completely obscured (at roughly \( \dot{M}_\text{w} \sim \text{few } \times 10^{-6} M_\odot/\text{yr} \) in our default model, see Figure 2). At this point, the ionised medium becomes confined within the neutral outer layers of the wind, and forbidden lines begin to appear as well, produced at the interface of the ionised and neutral gas. At \( \dot{M}_\text{w} \gtrsim 3 - 5 \times 10^{-6} M_\odot/\text{yr} \), the Ly\( _{\alpha} \) luminosity of the gas cloud reaches \( \sim 10\% \) of the total luminosity of the central source.

Rappaport et al. (1994) modelled the effect of persistent, unobscured, super-soft X-ray sources on the sur-
rounding (low density) interstellar medium. Their results showed that such sources should develop parsec-sized ionisation nebulae which would exhibit strong emission in forbidden optical lines, most importantly [O III] 5008Å, as well as in recombination lines of hydrogen and helium, including He II 4686Å. They suggested using forbidden oxygen lines ([OII] and [OIII]) as a diagnostic tool to find ionised ISM nebulae around unobscured super-soft X-ray sources (Rappaport et al. 1993; Di Stefano et al. 1993). Much higher gas densities in the wind (∼ 10^9 cm^-3 in the wind vs. ∼ 1 cm^-3 in the ISM) make forbidden lines much weaker in our case. Figure 10 shows a comparison of the [OIII] 5007Å and HeII 4686Å to Hβ line ratios in the case of the obscuration by the wind with those expected from the ionisation nebula computed by Rappaport et al. (1994) (their Figure 5). As one can see from the plot, a super-soft source obscured by the dense wind considered in this work will be easily distinguishable from the case of the ionised nebula around a super-soft source imbedded in the low density ISM.

To conclude, the observational signatures of a fully obscured super-soft X-ray sources should be significant (up to ∼ 10^37 erg/s for a 10^38 erg/s source) Lyα emission, coupled with the low [OIII]-to-Hβ ratio, of ∼ 10^{-2}, and relatively high HeII 4686Å-to-Hβ ratio, ∼ 1. These characteristics make obscured super-soft sources an observationally distinct class of compact line emission sources.

4.2 The inner wind radius

The critical mass-loss rate at which obscuration of the central source becomes significant shows moderate dependence on the assumed inner radius of the wind. Eq. 5 predicts that \( M_{\text{w,crit}} \propto r_{\text{inn}}^{1/2} \), whereas numerical calculations with Cloudy show marginally stronger scaling. The moderate \( r_{\text{inn}} \)-dependence is a consequence of the two assumptions made in our calculations: (i) that the \( \rho_{\text{gas}} \propto r^{-2} \) density profile extends to infinitely small radii and (ii) that the source of radiation is located in the locus of this density distribution, i.e. at the point \( r = 0 \). These two assumptions combined together lead to the strong dependence of the total recombination rate in the gas shell on its inner radius, eq. 4. To eliminate these assumptions, one would need to specify the driving mechanisms behind the mass loss and accurately consider the physical conditions at the inner wind boundary, which is far beyond the scope of this work. Below we consider the example of symbiotic systems to attribute some physical meaning to the inner radius in our simulations.

Recent modelling of the red giant winds (Suzuki 2007) demonstrated that the \( \rho_{\text{gas}} \propto r^{-2} \) density profile may indeed be a valid representation of the wind structure down to rather small radii, as low as ∼ 0.1 AU. The source of ionising radiation (i.e. the white dwarf), however, is offset by the distance \( a \) (binary separation) from the singular point of the gas distribution. In the absence of the singularity, the dependence of the total recombination rate in the gas shell on its inner radius is insignificant (as long as \( r_{\text{inn}} \ll r_{\text{out}} \)) and the only role of the \( r_{\text{inn}} \) in this case is to provide the normalisation of the density distribution, via the mass continuity equation \( \dot{M}_{\text{w}} = 4 \pi r^2 \rho(r) u_w \). Therefore it is natural to set \( r_{\text{inn}} = a \) in this case, i.e. the inner radius is of the order of the orbital separation in the binary system. Note also, that the 3-dimensional nature of the problem becomes essential at \( r \sim a \), as the red giant will be casting a shadow onto the wind material located behind it. Obviously, the simplified 1-dimensional consideration in this paper is applicable only to the lines of sight which are not passing close to the donor star.

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3 A caveat here is that such a nebula has been so far detected only around one super-soft source (Remillard et al. 1993; Woods & Gilfanov 2015).
To conclude, while the picture of a spherical shell confined between the inner and outer boundaries is a simplification of the real geometry of a circumbinary gas cloud, our model is a useful first approximation. This is the geometry considered in the previous work (Nielsen et al. 2013) and its use here facilitates comparison with those results and helps to isolate the effect of photo-ionisation. Future work (currently in progress) will aim at dealing with more realistic density structures and source spectra than those discussed here.

5 CONCLUSIONS

We have presented full photo-ionisation simulations of the interaction between the radiation from a super-soft X-ray source and a circumbinary cloud of Solar metallicity gas. This seeks to model a single-degenerate system that has lost material from either the donor or the accretor into the circumbinary region. The aim has been to determine the amount of material (parametrised by a circumstellar mass-loss rate) required to significantly obscure the X-ray emission from the accretor.

To simulate the effect of the X-ray source on the gas cloud we used the one-dimensional photo-ionisation code Cloudy (Ferland et al. 2013). Our analysis explored intervals of source temperature, luminosity, inner and outer radii of the gas cloud, and wind velocity, to cover the range of values for realistic systems.

We found that the amount of circumstellar matter required to hide a super-soft X-ray source from our current observational capabilities is about an order of magnitude larger than that found in Nielsen et al. (2013). In particular, the required mass-loss rates from the binary typically exceed $10^{-7}$ to a few times $10^{-6}$ $M_\odot$ yr$^{-1}$ for the parameters considered in the 'default' case in this work. Since the donor star has to provide both the material being accreted onto the white dwarf (and hence powering its X-ray emission) and the circumstellar material, this places significant constraints on the mass of the donor star.

We discussed the observational appearance of hypothetical nuclear burning white dwarfs obscured by a wind. Such systems would appear as luminous ($\sim 10^{37}$ erg/s) compact sources of Ly$\alpha$ emission with strong HeII recombination lines (HeII 4686Å to H$\beta$ ratio $\sim 1$ and suppressed forbidden lines of metals, e.g. [OIII]-to-H$\beta$ ratio, of $\sim 10^{-2}$), making them distinct from photo-ionised nebulae predicted to exist around super-soft X-ray sources imbedded in the low density ISM.

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