Study on Thermophysical Properties of a Lead–Bismuth-Based Graphene Nanofluid

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Incorporating graphene nanoparticles with high thermal conductivity into a lead-based coolant can significantly increase its thermal conductivity and specific heat capacity, thereby increasing the core power density of lead–bismuth cooled reactors, reducing the amount of coolant required, and ultimately realizing a miniaturized and lightweight reactor design. The purpose of the design is of great significance to the engineering application of lead–bismuth stacks in remote areas and open seas. In this study, the thermophysical properties of metal-based graphene nanofluids are analyzed by comparing and analyzing prediction models established for the thermal conductivity, viscosity, and specific heat capacity. The strengthening mechanism of nanofluids is summarized, and a series of suitable calculation formulae for the thermophysical properties of lead–bismuth-based graphene nanofluids is proposed. The research results show that incorporating graphene nanoparticles into a lead–bismuth-based coolant can significantly improve its thermal conductivity and specific heat capacity. When the nanoparticle suspension is relatively stable, the thermal conductivity, specific heat capacity, and viscosity increase significantly with the concentration of graphene nanoparticles. When the concentration reaches 20%, the thermal conductivity and specific heat capacity of the nanofluid are enhanced by approximately 80 and 20%, respectively, whereas the viscosity is also increased by approximately 100%. Therefore, it is important to appropriately select the parameters for the addition of nanoparticles to maximize the effect of lead–bismuth-based graphene nanofluids on the heat transfer performance of the reactor core.

Keywords: lead-bismuth cooled reactor, graphene nanofluid, thermal conductivity, viscosity, specific heat capacity

INTRODUCTION

High-performance lead–bismuth cooled reactor technology characterized by miniaturization and weight reduction is expected to change the mode of remote energy supply. The abundant energy supply provided by such reactors can fundamentally reduce or eliminate the need for logistics and other infrastructure related to energy equipment, bringing about an innovative development of nuclear power equipment. High-performance lead–bismuth cooled reactor technology has broad application prospects in military and civilian fields such as in nuclear-powered ships, nuclear-powered missiles, land-based mobile nuclear power supplies, underwater nuclear energy networks, nuclear-powered torpedoes, offshore drilling platforms, and deep-sea operation equipment capabilities. Minimizing the volume and weight of the reactor can help significantly improve the flexibility and maneuverability of nuclear power plants while ensuring sufficient power supply. For
TABLE 1 | The properties of graphene nanoparticles.

| Properties | Density (g/cm³) | Thermal conductivity (W/(m K)) | Specific heat capacity (J/(kg K)) | Melting points (°C) | Boiling points (°C) |
|------------|----------------|-------------------------------|----------------------------------|--------------------|--------------------|
| Values     | 2.25           | 2000–5,300                    | 710                              | 4,125              | 4,827              |

TABLE 2 | Thermal conductivity calculation models for nano fluids.

| Models          | Expressions                                                                 | Remarks                                      |
|-----------------|-----------------------------------------------------------------------------|----------------------------------------------|
| Maxwell         | \( \frac{C_{p}}{k_{p}} = \frac{4}{9} \left( \frac{1 - 6\eta_{p}}{1 + 6\eta_{p}} \right) \) | Suitable for spherical particles             |
| Hamilton–Crosse | \( \frac{C_{p}}{k_{p}} = \frac{4}{9} \left( \frac{1 - 6\eta_{p}}{1 + 6\eta_{p}} \right) \) | Suitable for spherical and subspherical particles |
| Leal            | \( \frac{C_{p}}{k_{p}} = \frac{4}{9} \left( \frac{1 - 6\eta_{p}}{1 + 6\eta_{p}} \right) \) | Considers the influence of Brownian force on thermal conductivity |
| Xuan(a)         | \( \frac{C_{p}}{k_{p}} = \frac{1 + \eta_{p}(1 + 0.028 \frac{\phi}{\phi_{p}}) \rho_{p}}{\eta_{p}} \) | Considers factors such as nanoparticle volume fraction, particle size, and temperature |
| Xuan(b)         | \( \frac{C_{p}}{k_{p}} = \frac{1 + \eta_{p}(1 + 0.028 \frac{\phi}{\phi_{p}}) \rho_{p}}{\eta_{p}} \) | Considers nanoparticle agglomeration and surface adsorption |
| Chu             | \( \frac{C_{p}}{k_{p}} = \frac{1 + \eta_{p}(1 + 0.028 \frac{\phi}{\phi_{p}}) \rho_{p}}{\eta_{p}} \) | Considers volume fraction, length, interface thermal resistance, and flatness |
| Kedar          | \( \frac{C_{p}}{k_{p}} = \frac{1 + \eta_{p}(1 + 0.028 \frac{\phi}{\phi_{p}}) \rho_{p}}{\eta_{p}} \) | Considers interface thermal resistance and Brownian motion |

TABLE 3 | Viscosity calculation models for nano fluids.

| Model           | Expressions                                                                 | Remarks                                      |
|-----------------|-----------------------------------------------------------------------------|----------------------------------------------|
| Einstein        | \( \frac{C_{v}}{f_{v}} = \frac{1 + 2.5 \eta}{(1 + \eta)^{2.5}} \)          | Suspension of spherical particles             |
| Brinkman        | \( \frac{C_{v}}{f_{v}} = \frac{1 + 2.5 \eta}{(1 + \eta)^{2.5}} \)          | Considers the interaction between particles |
| Batchelor       | \( \frac{C_{v}}{f_{v}} = 1 + 2.5 \eta + 6.5 \eta^{2} \)                  | Considers the influence of Brownian motion |
| Kreger–Dougherty| \( \frac{C_{v}}{f_{v}} = \frac{1}{(1 + \eta)^{2.5}} \)                     | Spherical particle suspension under high shear rate |
| Thomas          | \( \frac{C_{v}}{f_{v}} = \frac{1 + 2.5 \eta + 10.05 \eta^{2} + 0.00273 \eta^{3}}{1 + 3.48(1 + \eta)} \) | Spherical particles with higher concentration |
| Massimo         | \( \frac{C_{v}}{f_{v}} = \frac{1}{1 - 3.48(1 + \eta)} \)                   | Considers the influences of base fluid viscosity, particle concentration, and particle size |

TABLE 4 | Specific heat capacity calculation models for nano fluids.

| Models | Expressions                                                                 | Remarks                                      |
|--------|-----------------------------------------------------------------------------|----------------------------------------------|
| Pak    | \( C_{sp} = (1 - \phi) C_{sp} + \phi C_{sp} \)                              | Based on the ideal gas mixture mixing concept |
| Xuan   | \( C_{sp} = \frac{1 + \phi (C_{sp} - C_{sp})}{1 + \phi (C_{sp} - C_{sp})} \) | Considers the influence of density          |
| Shin   | \( C_{sp} = \frac{\rho_{sp} C_{sp} + \rho_{sp} C_{sp} + \rho_{sp} C_{sp}}{\rho_{sp} + \rho_{sp} + \rho_{sp}} \) | Considers the influences of density and semi-solid layer |
|        | \( C_{sp} = \frac{\rho_{sp} C_{sp} + \rho_{sp} C_{sp} + \rho_{sp} C_{sp}}{\rho_{sp} + \rho_{sp} + \rho_{sp}} \) | Based on the assumption that the semi-solid layer thickness is 1 nm |

High-performance lead–bismuth cooled reactors, the amount of coolant in the primary loop is a major factor influencing the volume and weight of the reactor, and it is an important research parameter for reactor performance optimization (Li et al., 2020). To enhance the heat transfer ability of a lead–bismuth coolant, graphene nanoparticles can be added to further improve its thermal conductivity and heat exchange capabilities, thus realizing high-performance lead–bismuth-based graphene nanofluids. The properties of graphene nanoparticles are shown in Table 1 (Lei and Zhang, 2017). A lead–bismuth-based graphene nanofluid can increase the core power density of high-performance lead–bismuth cooled reactors and reduce the amount of coolant required in the primary cooling system of the reactor, ultimately achieving a miniaturized and lightweight design of the reactor.

The basic concept of nanofluids was first conceived by Choi and Eastman (1995) by adding nanoscale solid particles into a base solution, the heat conductivity of the solution can be significantly improved. Qiao (2010) carried out experiments on the preparation and performance of graphene nanofluids and proposed a suitable prediction model. Yimin (2014) studied the heat conduction and heat exchange enhancement mechanisms of nanofluids and proposed a thermal conductivity model considering nanofluid aggregation structures. Shu (2019) studied the thermal properties and heat transfer of water-based graphene nanofluids. Shukla et al. (2016) proposed a new calculation model for the thermal conductivity coefficient of nanofluids with spherical and non-spherical shapes based on Brownian motion. Demirkır and Erteşk (2020) studied the rheological characteristic and thermal properties of water-
based graphene nanoﬂuids. The above results have shown that nanoparticles can help significantly improve the thermophysical properties of the base fluid.

However, conventional nanometer-sized particles dispersed in water or ethylene glycol as the base fluid easily form sediments and affect the stability of the suspension because of the signiﬁcant difference in the speciﬁc densities between the base fluid and the particles, which limits the ability to enhance the heat transfer of the fluid. Ma and Liu (2007) proposed to use a liquid metal or a low-melting alloy as the heat transfer medium to cool computer chips and further analyzed their use as the base fluid with graphene nanoparticles, which were added to the liquid metal alloy to introduce the concept of an “ultimate coolant” with ultra-high thermal conductivity. Men (2010) studied a liquid metal-based nanoﬂuid as a heat transfer medium using a single-phase ﬂuid model, a discrete phase model, and a Eulerian–Eulerian (E–E) model to study its ﬂow and heat transfer effect under forced convection-based natural convection. Zhou et al. (2020) used metal gallium as the base liquid and added alumina (Al2O3), diamond, and carbon nanotubes as nanoparticles to study the inﬂuence of the nanoparticles on the heat transfer performance of the base metal liquid. The results showed that when Re = 1,000 and φ = 6%, the Nusselt numbers of the nanoﬂuids Ga–CNT, Ga–Diam, and Ga–Al2O3 could be enhanced by 17.3, 16.1, and 2.1%, respectively, compared with that of pure liquid metal Ga. A nanoparticle ﬂuid with a high concentration of graphene nanoparticles is the best choice for heat transfer enhancement.

Current research on graphene nanoﬂuids mainly involves conducting experiments and model predictions at normal temperatures. Few studies have been performed under high-temperature and high-heat-ﬂux conditions, and the mechanism whereby nanoparticles improve the thermal conductivity and speciﬁc heat capacity of the ﬂuid has not been thoroughly investigated. The proposed model of the mechanism cannot be widely applied to scenarios where different types of nanoparticles improve the thermophysical properties of the ﬂuid. Therefore, this study uses high-temperature lead–bismuth liquid metal as the base liquid and compares it with sodium, gallium, and other liquid metals to study the effects of the concentration, temperature, particle size, and other factors on the thermal conductivity, viscosity, and speciﬁc heat capacity. A prediction model for the thermal conductivity, viscosity, and speciﬁc heat capacity of a graphene-based nanoﬂuid is established, laying a theoretical foundation for the subsequent application of lead–bismuth-based graphene nanoﬂuids as the cooling medium in lead–bismuth cooled reactors.

**FACTORS AFFECTING THE STABILITY OF LEAD–BISMUTH-BASED GRAPHENE NANOFLUIDS**

A certain amount of nanoparticles was added to the base liquid to form nanoﬂuids. Nanoparticles, due to their small-scale effect, irregular Brownian motion, and strong surface effect, form agglomerates with a number of weakly connected interfaces and then precipitate, ultimately affecting the stability of the nanoﬂuid. Therefore, the basis for studying the thermophysical properties of nanoﬂuids is to ensure their uniform and stable distribution in the base ﬂuid without agglomeration. The resultant force experienced by the nanoparticles can be expressed as in Eq. 1 (Agarwal et al., 2013):

\[
F_F = F_b + F_t + F_a + F_s + F_R
\]

where \(F_b\) is the Brownian force experienced by the nanoparticles, \(F_t\) is the buoyancy force; \(F_s\) is the interphase resistance; \(F_a\) is the van der Waals force; \(F_R\) is the electrostatic repulsion force.

The mass force on the nanoparticles can be temporarily ignored due to their nanometer size. Only the van der Waals force and the electrostatic repulsion force on the nanoparticles are considered. The force analysis shows that the stability of the nanoﬂuid depends on the relative magnitude of the repulsive and suction forces. When the repulsion force is greater than the suction force, the Brownian motion causing nanoparticle collisions can be sufﬁciently prevented so as to avoid agglomeration and precipitation. Adjusting the balance between the suction and repulsion of the suspended nanoparticles by different means can keep the suspension in a stable state for a longer time. Based on the type of repulsive force, the repulsive force experienced by the dispersed nanoparticles can be divided into spatial repulsion and charge repulsion, as shown in Figure 1 (Balanta et al., 2011).

From a microscopic viewpoint, the inﬂuence of nanoﬂuid stability mainly includes three aspects (Wu et al., 2020): 1) There are multiple dispersion systems in the nanoﬂuids. Nanoparticles have a large speciﬁc surface area and high surface energy. They tend to agglomerate with each other, which reduces their surface energy. 2) The small-scale effect, irregular Brownian motion, and the resulting collisions between nanoparticles cause uneven forces and settlement. 3) Nanoparticles are prone to agglomeration under the action of electrostatic repulsion and spatial repulsion. Once agglomeration occurs, the surrounding nanoparticles in the suspension will also be adsorbed and agglomerated, thereby affecting the stability of the nanoﬂuid. Based on the aforementioned micromechanism analysis and experimental research, the factors affecting the stability of nanoﬂuids mainly include the particle density, particle shape, ﬂuid viscosity, dispersant, and pH value. The
above factors often affect the thermal conductivity, specific heat capacity, and other thermophysical properties.

**THERMAL CONDUCTIVITY OF LEAD–BISMUTH-BASED GRAPHENE NANOFUID**

The thermal conductivity is an important thermophysical property of lead–bismuth-based graphene nanofluids. Numerous research results have shown that nanoparticle addition can help significantly improve the thermal conductivity of fluids. The mechanism whereby nanoparticles improve the thermal conductivity of the base fluid can be mainly divided into the following four aspects.

**Thermal Conduction Mechanism of Nanofluid**

**Brownian Motion and Micro Convection Effect of Nanoparticles**

According to the Brownian motion theory (Einstein, 1956), nanoparticles suspended in a liquid are affected by the surrounding liquid molecules, and the particles keep moving randomly. The smaller the particle size, the higher the movement speed and the more frequent the movement; hence, the frequency of energy exchange between the nanoparticles and the fluid is higher, thereby improving the thermal conductivity of the fluid.

**Agglomeration and Percolation Structure of Nanoparticles**

In the process of energy transfer in the nanofluids, the ideal state is when the nanoparticles can be uniformly distributed in the base fluid at a relatively high concentration without agglomeration (Wang et al., 2012). In fact, the nanoparticles collide with each other in the base fluid because of their irregular Brownian motion, easily leading to agglomeration and large-cluster formation. The speed of these agglomerates is lower than those of the individual particles. The greater vertical force will accelerate the precipitation of the particles. The agglomeration phenomenon will reduce the energy transfer rate inside the nanofluid and reduce the enhanced heat transfer performance.

**Theoretical Studies on Liquid Layer Formed by Nanoparticles and Base Liquid**

Based on experimental observations, researchers have found that an ordered liquid layer nanostructure is formed around the nanoparticles. This solid-like structure plays a leading role in the thermal conduction process from solid to liquid, which increases the effective thermal conductivity of the nanofluid. The thickness can be given as follows (Ma, 2008):

$$d_s = \frac{1}{\sqrt{3}} \left( \frac{4M}{\rho_f N_A} \right)^{\frac{1}{3}} \quad (2)$$

where $M$ is the mass fraction of the liquid, $\rho_f$ is the density of the liquid, and $N_A$ is Avogadro’s constant ($6.022 \times 10^{23}$/mol).

From the formula, find that the thickness of the nanostructure is only related to the base fluid. The other influencing factors need to be continuously improved, and whether the main heat conduction mechanism of the liquid layer is solid heat conduction or liquid heat conduction requires further research.

**Ballistic Transport and Nonlocal Effect**

A ballistic transport phenomenon occurs when the nanoparticle diameter is smaller than the free path of the phonon and when there is no scattering inside the molecule. At this time, the internal thermal conductivity of the nanoparticle is insufficient. The diffusion capacity at the liquid interface is dominant. However, some experimental results have shown that this local effect cannot explain the improved thermal conductivity of nanofluids (Nie et al., 2008).

**Thermophoresis Theory**

Thermophoresis is due to the existence of a temperature gradient. The molecules on the high-temperature side are impacted more strongly than those on the low-temperature side, leading to a directional movement of the molecules. However, experiments have shown that this phenomenon has largely no influence on the thermal conductivity of nanofluids and that it is several orders of magnitude lower than the effect produced by Brownian motion (Koo and Kleinstreuer, 2005).

**Radiation Heat Transfer**

From a molecular dynamics simulation, the energy transfer speed between two particles increases sharply when the distance between them is $< 1 \mu$m. Therefore, it can be considered that near-field radiation may have a greater effect on thermal conductivity. However, some researchers pointed out that near-field radiation does not significantly enhance the heat conduction of nanofluids, even when the intensity of near-field radiation is greater than that of blackbody radiation (Koo and Kleinstreuer, 2005; Ben-Abdallah, 2006).

Figure 2 shows the schematic of each theory (Zhao et al., 2013).

**Thermal Conductivity Calculation Model**

Based on the aforementioned heat conduction and heat transfer mechanism, domestic and foreign scholars have established a thermal conductivity calculation model for nanofluids.

In 1873, Maxwell (1904) studied the mechanism whereby small solid particles added to a liquid improve the thermal conductivity ability and provided a solid–liquid two-phase flow basic heat conduction model. Thereafter, scholars mainly improved and revised this theoretical model. Although the basic model does not accurately predict the thermal conductivity of solid–liquid fluids, the law of thermal conductivity has been verified by subsequent experiments.

$$k_{eff} = \frac{k_p + 2k_f - 2\varphi(k_f - k_p)}{k_p + 2k_f + 2\varphi(k_f - k_p)} \quad (3)$$

where $k_p$ is the thermal conductivity of the particles, $k_f$ is the thermal conductivity of the liquid, and $\varphi$ is the volume fraction of the particles.
Wu and Zhao (2013) analyzed the effects of the size and shape of nanoparticles on the thermal conductivity of nanofluids and proposed that the thermal conductivity of slender-particle nanofluids is much higher than those of spherical nanoparticles. Nanoparticles that are uniformly dispersed have a higher thermal conductivity.

Hamilton and Crosser (1962) proposed the H-C thermal conductivity model for the effect of the nanoparticle shape on the thermal conductivity of the suspension:

\[
\frac{k_{\text{eff}}}{k_f} = \frac{k_p + (m - 1)k_f - (m - 1)\psi(k_f - k_p)}{k_p + (m - 1)k_f + \psi(k_f - k_p)}
\]

where \( m \) is the shape factor, \( m = 3/\psi \), \( S_V \) is the surface area of the spherical particle with the same particle volume, and \( S_p \) is the surface area of the particle.

Leal (1973) proposed a model for the thermal conductivity of spherical particles with a solid-liquid two-phase flow. This model fully considers the influence of the Brownian force on the thermal conductivity of the suspension.

\[
k_{\text{eff}} = 1 + \psi \left[ \frac{1.176(k_p - k_f)^2}{(k_p + 2k_f)^2} + 5 \left( \frac{0.6 - 0.028k_p - k_f}{k_p + 2k_f} \right) \right] Pe_f^{3/2}
\]

where \( Pe_f = r^2 \rho c_p \gamma / k_f \), where \( r \) is the particle radius, \( \gamma \) is the velocity gradient, \( \rho \) is the density, and \( c_p \) is the specific heat capacity.

Yimin (2014) studied nanoparticle molecular dynamics and micromolecular heat transfer process, comprehensively considered the volume fraction, particle size, base fluid temperature, interface thermal resistance, and other factors of the nanoparticles, proposed a thermal conductivity calculation model for the nanofluid:

\[
\frac{k_{\text{eff}}}{k_f} = \frac{k_p + 2k_f - 2\psi(k_f - k_p)}{k_p + 2k_f + \psi(k_f - k_p)} + \frac{18\psi H \kappa \beta T}{\pi^2 \rho d_p^6 r} \tag{7}
\]

where \( H \) is the total heat transfer coefficient; \( T \) is the fluid temperature; \( A \) is the heat transfer surface area; \( d_p \) is the particle size; \( k_B \) is the Boltzmann’s constant, and \( \tau \) is the relaxation time constant.

Later, Yimin et al. (2002) proposed a thermal conductivity calculation model for the agglomeration of nanoparticles considering the characteristics of nanoparticle agglomeration in the base fluid. Notably, this model ignores the effect of the interface thermal resistance on the thermal conductivity:

\[
k_{\text{eff}} = \frac{k_p + 2k_f - 2\psi(k_f - k_p)}{k_p + 2k_f + \psi(k_f - k_p)} + \frac{\rho_p \psi C_p}{2k_f} \sqrt{\frac{k_f T}{3\tau r \mu}} \tag{8}
\]

where \( \rho_p \) is the particle density, \( C_p \) is the specific heat capacity of the particle, \( \psi \) is the particle volume fraction, \( r_c \) is the particle radius, and \( \mu \) is the dynamic viscosity of the fluid.

Chu et al. (2013) established a calculation model for the thermal conductivity of graphene nanofluids, as expressed in Eq. 9. This model fully considers the volume fraction, thickness, length, interface thermal resistance, and particle flatness of
graphene nanoparticles. However, in different base fluid systems, the interface thermal resistance and flatness of the nanoparticles need to be measured experimentally, which makes this model more uncertain.

$$k_{\text{eff}} = \frac{3 + 2\eta^2\psi}{k_f} \left[ \frac{2w}{6\psi} + 13.4\sqrt{T} \right] \frac{3 - \eta\phi}{\psi} \left( \frac{\pi}{\pi N_u} \right)^{-1}$$

(9)

where $\eta$ is the flatness of the graphene nanoparticles, $R_k$ is the interface thermal resistance, $L$ is the length of the particle, and $t$ is the thickness of the particles.

Shukla et al. (2016) provided a thermal conductivity model of the nano fluid considering Brownian motion, as expressed in Eq. 10. This model considers the interface thermal resistance of the particles and the microenergy transfer due to Brownian motion.

$$k_{\text{eff}} = \frac{1 - \varphi}{k_f} + \varphi \left[ \frac{k_p}{k_f} \left( \frac{\pi}{6\varphi} \right)^{1/3} \times \psi \left( \frac{\pi N_u}{\pi N_u} \right)^{-1} \right]$$

(10)

where $\psi$ is the sphericity of the nanoparticles, and its value for spherical particles is 1. $k_p$ is the thermal conductivity of the particle, $k_f$ is the thermal conductivity of the fluid, and $\varphi$ is the volume fraction of the particles. $N_u = f(Re, Pr)$, where $Re$ is the Reynolds number, and $Pr$ is the Prandtl number; when the nanoparticles are relatively static with respect to the base fluid, $Pr < 1$ and $Re \ll 1$; at this time, the Nusselt number $N_u$ can be 2.

The thermal conductivity calculation model of nano fluid is organized as shown in Table 2.

Fully considered the theoretical mechanism and theoretical calculation model for the thermal conductivity of nanofluids and analyzed the factors affecting the nanofluids. Taking spherical nanoparticles as an example, selected different thermal conductivity theoretical calculation models and carried out the calculation process, with the volume fraction of the nanoparticles set in the range of 0–20%. Figure 3 shows the calculation result.

The results show that the selected models can reflect the change law of the thermal conductivity of the nanofluids with respect to the nanoparticle concentration, with the prediction made by Xuan model’s tending to be higher. From the experimental result, recommending using the theoretical calculation model proposed by Xuan et al., which considers the occurrence of agglomeration. This model is based on Maxwell’s model. It fully considers the laws of molecular dynamics and thermodynamics and theoretically reflects accurately the thermal conductivity of lead–bismuth-based graphene nanofluids. The variations in the thermal conductivity with the concentration, temperature, and particle size of the graphene nanoparticles were studied separately, and experimental simulation calculations were carried out. The results were compared with lead–bismuth (LBE), sodium, and gallium as base fluids, as shown in Figures 4–6:

The results indicate that the specific thermal conductivity of the nanofluid improves with the increase in the concentration, and the thermal conductivity of the lead–bismuth-based liquid is greater than those of sodium and gallium. When the concentration reaches 20%, the thermal conductivity of the LBE base fluid increases by 80%. The thermal conductivity of the nanofluids improved with increasing temperature, whereas the change with temperature is relatively gentle. When considering the influence of temperature on the nanofluids, it
can be considered as a factor. Under similar temperature conditions, the thermal conductivity of lead–bismuth-based nanofluids is greater than those of sodium and gallium. The thermal conductivity of nanofluids decreases with increasing particle size, and when the particle size is sufficiently small, the thermal conductivity decreases rapidly with increasing
When the diameter of the subsequent nanoparticles (approximately 500 nm) increases or when they form agglomerates, the effect of the particle size on the thermal conductivity can be ignored. The thermal conductivity of the nanofluid is sensitive to changes in the concentration. To improve the thermal conductivity of the nanofluid, the volume fraction of the nanoparticle can be increased as much as possible under the premise of keeping the nanoparticle suspension stable.

**VISCOSITY OF LEAD–BISMUTH-BASED GRAPHENE NANOFLUIDS**

Rheological properties are vital to the heat transfer process of nanofluids. The rheological properties of nanofluids directly affect their heat transfer ability. Adding nanoparticles can help increase their viscosity. The volume concentration of the nanoparticles increases to a certain extent, and the fluid properties of the nanofluids will change from Newtonian to non-Newtonian. At this time, the fluid heat transfer is unfavorable (Aiguo et al., 2017).

The particle concentration, particle shape, particle size, base fluid density, and base fluid temperature affect the viscosity of nanofluids. The expression for the nanofluid viscosity is as follows:

$$\mu_{\text{eff}} = f(\mu_f, \varphi, r, K, \xi, T)$$  \hspace{1cm} (11)

where $\mu_f$ is the viscosity of the fluid, $\varphi$ is the volume fraction of the nanoparticles, $r$ is the particle size, $K$ is the particle shape coefficient, $\xi$ is the electromotive force, which represents the electroviscous effect, and $T$ is the temperature.

A nanofluid is essentially a special solid–liquid two-phase suspension system. Most scholars combined the classic suspension system viscosity ball theory model proposed by Einstein in 1906 (Einstein, 1905), combined with experiments to predict the law of viscosity change of nanofluids. The small-sphere model assumes that spherical particles are uniformly suspended in a dilute linear viscous fluid and that the suspended particles are rigid spheres with no charge on the surface or any interaction. The viscosity of the nanofluid can be expressed as:

$$\frac{\mu_{\text{eff}}}{\mu_f} = 1 + 2.5\varphi$$ \hspace{1cm} (12)

where $\varphi$ is the volume fraction of the nanoparticles.

Brinkman (1952) considered the interaction between particles on the basis of Einstein’s model, with the applicable range of the volume fraction extended to 4%. Brinkman’s model can be expressed as:

$$\frac{\mu_{\text{eff}}}{\mu_f} = (1 - \varphi)^{-2.5}$$ \hspace{1cm} (13)

Batchelor (1977) assumed that a nanofluid is a suspension of isotropic rigid spheres, considered the influence of Brownian motion, and proposed the following model:

$$\frac{\mu_{\text{eff}}}{\mu_f} = 1 + 2.5\varphi + 6.5\varphi^2$$ \hspace{1cm} (14)

Krieger and Dougherty (1959) proposed a semi-empirical formula assuming a spherical particle suspension at a high shear rate, which can be expressed as:
\[
\frac{\mu_{\text{eff}}}{\mu_f} = \left(1 - \frac{\varphi}{\varphi_m}\right)^{-2.5 \varphi_m}
\]  \hspace{1cm} (15)

where \(\varphi_m\) is the maximum volume fraction, which is approximately a constant of 0.605.

Thomas et al. (Su et al., 2013) proposed a viscosity calculation formula suitable for spherical particles with a high particle volume concentration.

\[
\frac{\mu_{\text{eff}}}{\mu_f} = 1 + 2.5 \varphi + 10.05 \varphi^2 + 0.00273 e^{16.6 \varphi}
\]  \hspace{1cm} (16)

Based on the influences of the base fluid viscosity, particle concentration, and particle size on the viscosity of nanofluids, Corcione (2011) derived a formula for calculating the viscosity when the nanoparticle size is in the range of 25–200 nm.

\[
\frac{\mu_{\text{eff}}}{\mu_f} = 1 - 34.87 \left(\frac{d_p}{d_f}\right)^{0.3} \varphi^{1.5}
\]  \hspace{1cm} (17)

\[
d_f = 0.1 \left(\frac{6M_{\text{b}}}{N_A \rho_{\text{f}0}}\right)^{1/3}
\]  \hspace{1cm} (18)

where \(d_p\) is the nanoparticle diameter, \(M\) is the molar weight of the liquid, \(N_A\) is Avogadro’s constant, and \(\rho_{\text{f}0}\) is the density of the base liquid at 303.15 K.

The viscosity calculation model of nanofluids is organized as shown in Table 3.

Figure 7 shows the variation in the nanofluid viscosity with the concentration obtained using the above viscosity calculation model. As shown, the Massimo model is only suitable when the nanoparticle concentration is low. Other models reflect the effect of nanoparticle concentration on the viscosity of nanofluids, this is, the concentration of nanofluid increases with increase in the volume fraction of the nanoparticles. The improvement in viscosity is twofold when the concentration reaches 20%. To better predict the viscosity of higher-concentration lead–bismuth-based graphene nanofluids, the more accurate Thomas model can be selected.

For the relationship between the viscosity of the metal fluid and the temperature variation, the Vogel-Fulcher-Tammann (VFT) formula is commonly used (Xie et al., 1988). This formula can predict the nanofluid viscosity with temperature variation.

\[
\eta = \eta_0 e^{\frac{A}{T-T_0}}
\]  \hspace{1cm} (19)

where \(\eta_0\), \(T_0\), and \(A\) are specific parameters. Taking the logarithm on both sides of Eq. 19, finding that \(ln\eta\) has a linear relationship with \(1/(T-T_0)\).

The viscosity of graphene nanofluid decreases with the increase in the temperature at low concentrations. Figure 8 shows its variation law, which is the same as the variation trend in the viscosity of the base fluid. With the increase in the concentration of graphene nanoparticles, the interaction force between the base fluid and the particles increases, thereby increasing the fluid viscosity.

**Figure 7** | Different models used to predict the change in the nanofluid viscosity with particle concentration (T = 600 K).
SPECIFIC HEAT CAPACITY OF LEAD–BISMUTH-BASED GRAPHENE NANOFLUID

The specific heat capacity is an important thermophysical property of reactor cooling fluids and represents the ability of a cooling medium to transfer and store heat. Pacheco et al. (Romero et al., 2002) reported that the specific heat capacity of conventional fluids must be higher than 2.25 J g⁻¹ K⁻¹ and should operate stably in the temperature range of 600–800°C in order to be competitive with fossil fuel-based energy in terms of pricing. For lead–bismuth cooled reactors, the specific heat capacity of the lead–bismuth base is relatively low, which is far from meeting this requirement. Improving the heat capacity of the lead–bismuth coolant can help reduce the amount of coolant required, decrease the volume of the body, and improve the heat storage capacity, heat transfer conductivity efficiency, and stability of the heat exchange system. Some researchers conducted extensive and in-depth studies on the heat capacity of nano fluids. A large number of experiments have proven that nanoparticles can effectively increase the specific heat capacity of the base fluid (Tiznobaik and Shin, 2013).

Specific Heat Capacity Enhancement Mechanism

Studies on the specific heat capacity enhancement mechanism of nano fluids have been mainly based on specific experimental characterization and calculation simulation prediction. Accordingly, researchers proposed three nanofluid specific heat capacity enhancement mechanisms (Ho and Pan, 2014):

1) Nanoparticles with higher specific heat capacity.

A higher specific heat capacity of the nanoparticles helps improve the specific heat capacity of the nanofluid. However, some researchers have pointed out that when SiO₂ nanoparticles are added to a base liquid of inorganic salts, such as nitrate, with a higher specific heat capacity, the specific heat capacity can also result in a higher strengthening effect than the base liquid. Therefore, the mechanism whereby the nanoparticles themselves improve the specific heat capacity remains to be discussed (Tian et al., 2020).

2) Specific surface energy of nanoparticles and thermal resistance of solid–liquid interface.

The specific surface area of nanoparticles is high because of their small-size effect; thus, the number of atoms on the surface accounts for the total number of atoms. More external atoms are active compared with the atoms close to the center because of the uneven force on the inside and outside, forming a higher vibration entropy. As a result, nanomaterials have a higher specific surface energy and specific heat capacity. The contact part between the nanoparticles and the base fluid has interface thermal resistance. The interface thermal resistance is higher because of its high specific surface area, which can bring additional heat storage. Thus, the specific heat capacity of the nanofluid is enhanced.

3) Formation of a semi-solid layer between the surface of the nanoparticle and the base fluid.

The surface of the nanoparticles adsorbs the molecules of the base fluid, and the liquid atoms form an aligned and ordered atomic
arrangement, resulting in the formation of a semi-solid layer structure. The intermolecular bonding is tight because of the formation of a structure similar to the crystal structure, resulting in a potential barrier phenomenon in the semi-solid. Sufficient energy must be absorbed to break away from the constraints of the nanoparticles, which will increase the specific heat capacity of the nanofluids.

**Calculation Model for Specific Heat Capacity**

Currently, most studies have concentrated on medium and low-temperature nanofluids, with few studies on the specific heat capacity of high-temperature and high-heat-flux nanofluids. The established nanofluid specific heat capacity calculation models can be described as follows:

Pak and Cho (1998) proposed a nanofluid specific heat capacity model in 1998. This model is based on the mixing concept of an ideal gas mixture, called a simple mixing model. The formula is as follows:

\[ C_{peff} = (1 - \varphi)C_{pf} + \varphi C_{pp} \]  

where \( \varphi \) is the volume fraction of the nanoparticles, and \( C_{peff}, C_{pf}, \) and \( C_{pp} \) are the specific heat capacities of the nanofluids, base fluids, and nanoparticles, respectively.

Xuan and Roetzel (2000) considered the density factor and proposed a correction formula for the specific heat capacity of nanofluids as follows:

\[ C_{peff} = (1 - \varphi)\left( \rho C_p \right)_j + \varphi \left( \rho C_p \right)_p \]  

where \( \rho C_p \) is the specific heat capacity of the base fluid, and \( \rho \) is the density of the base fluid.

Shin and Banerjee (2014) and the heat transfer mechanism of the specific heat capacity, a semi-solid layer with a thickness of approximately 1 nm can be formed on the surface of the nanoparticles. Based on a high-temperature molten salt base, a new high-temperature nanofluid specific heat capacity calculation model has been proposed as follows:

\[ C_{peff} = \frac{\varphi \rho \_p C_{pp} + \varphi \rho \_j C_{pf} + \varphi \rho \_s C_{ps}}{\varphi \rho \_p + \varphi \rho \_j + \varphi \rho \_s} \]  

The density of the semi-solid layer in this formula cannot be accurately measured using current observation and measurement data methods; therefore, the model needs to be improved and revised. Therefore, Shin et al. made the following assumptions: the thickness of the semi-solid layer structure was set to approximately 1 nm, and the density and specific heat capacity of the semi-solid were made equal to those of the nanoparticles. Based on the above assumptions, an improved specific heat capacity prediction model was proposed, as follows:

\[ C_{peff} = \frac{M_{c_{pp}} + \frac{M \rho \_p C_{ps}}{M} m_{bs} C_{ps} + \left( M - M \rho \_p - \frac{m_c}{M} m_{bs} \right) C_{pf}}{M} \]  

\[ m_p = \rho \_p V_p = \left( \rho \_p \pi D_p^2 \right) / 6 \]  

\[ m_{bs} = \rho \_bs V_{bs} = \rho \_bs \left( \frac{D_p^2 + \delta + d}{2} + \frac{D_p^2}{2} + d \right) \]  

where \( C_{peff}, C_{pp}, C_{ps}, \) and \( C_{pf} \) are the specific heat capacities of the nanofluid, nanoparticles, semi-solid layer, and base fluid, respectively; \( M, m_p, \) and \( m_{bs} \) are the total mass of the
nanofluid, the mass of the nanoparticles, and the mass of the semi-solid layer structure, respectively; $\varphi$ is the mass fraction of the nanoparticles; $\delta$ is the thickness of the semi-solid layer, and $d$ is the gap width.

Fakoor Pakdaman et al. (2012) obtained the calculation model of the specific heat capacity in the temperature range of 313–343 K based on the correlation formula of the least-squares method and combined with the experimental data.

Alade et al. (2020) applied the genetic algorithm/support vector regression (GA/SVR) model to accurately evaluate nanoparticles in the volume fraction range of 3.7–9.3%.

The calculation model of specific heat capacity of nano fluid is organized as shown in Table 4.

The above model is used to analyze and study the addition of lead–bismuth-based graphene, as shown in Figure 9.

Studies have shown that nanoparticles can help effectively increase the specific heat capacity of the lead–bismuth base. However, in the case of Xuan’s and Shin’s models, finding that the improvement in the specific heat capacity of graphene is limited, approximately 20%. Based on existing experimental research on the specific heat capacity of nano fluids, Shin’s model more accurately reflects the change law of the specific heat capacity with the concentration.

Currently, although there are many theories, experiments, and models on the specific heat capacity of nano fluids, they are limited to model prediction and theoretical analysis of specific experimental data. It is difficult to accurately measure microstructures such as of semi-solid layers and liquid separation surfaces. Accurate theoretical mechanism and calculation models are lacking. In particular, there are few research results on high-temperature nano fluids, such as metal bases, and further investigation is required.

**CONCLUSION**

This study combined related research progress in existing nano fluids and thermal properties of lead–bismuth-based graphene nano fluids for analysis, research, and calculation. The following conclusions can be drawn from the study results:

1) On the premise of ensuring the stability of the nano fluid, the thermal conductivity of the nano fluid increases with increasing nanoparticle concentration. The thermal conductivity of the fluid can be increased by 80% when the concentration reaches 20%. The thermal conductivity of the nano fluids improves with increasing temperature, though the increase degree is limited. As the particle size of the nanoparticles increases, or with the occurrence of agglomeration, the particle size of the agglomerates formed by nanoparticles becomes larger, and the thermal conductivity of the nano fluid decreases. The particle size increases to a certain extent, and the impact on the thermal conductivity can be ignored.

2) Nanoparticle concentration and fluid temperature are both important parameters influencing the viscosity of the nano fluids. The viscosity of the nano fluids increases with the increase in the concentration and decrease in temperature. However, the other parameters affecting the nano fluids can only be determined experimentally, and the theoretical model for the viscosity of nano fluids needs to be further studied.

3) The current strengthening mechanism of the specific heat capacity of liquids by nanoparticles is not perfect. The measurement technology used for the specific heat capacity of nano fluids at high temperatures needs to be improved. The existing calculation model is limited to specific experimental characterization, and the prediction model cannot accurately reflect the general law of specific heat capacity of nano fluids. In recent years, some scholars have tried to calculate and study the specific heat capacity of nano fluids through molecular dynamics simulations, which is a new research direction for the strengthening mechanism of nano fluids.

In short, nano fluid technology has broad practical prospects for enhancing the thermophysical properties of metals such as lead and bismuth. The addition of graphene to a lead–bismuth stack coolant can effectively improve all aspects of its thermal and physical properties, reduce the amount of coolant required, increase the thermal power density, and reduce the volume and weight of the lead–bismuth stack, making it possible to implement lead–bismuth stacks in remote areas and ocean environments, thus providing a solid theoretical foundation.

**DATA AVAILABILITY STATEMENT**

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

**AUTHOR CONTRIBUTIONS**

TY: Data curation, Writing—Original draft preparation. PZ: Supervision. QL: Conceptualization, Methodology. YZ: Visualization, Investigation. TY: Writing—Reviewing and Editing.

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