Privacy-Preserving Content-Based Image Retrieval in the Cloud

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Abstract—Storage requirements for visual data have been increasing in recent years, following the emergence of many new highly interactive multimedia services and applications for both personal and corporate use. This has been a key driving factor for the adoption of cloud-based data outsourcing solutions. However, outsourcing data storage to the Cloud also leads to new challenges that must be carefully addressed, especially regarding privacy. In this paper we propose a secure framework for outsourced privacy-preserving storage and retrieval in large image repositories. Our proposal is based on IES-CBIR, a novel Image Encryption Scheme that allows Content-Based Image Retrieval properties. Our solution enables both encrypted storage and searching using CBIR queries while preserving privacy. We have built a prototype of the proposed framework, formally analyzed and proven its security properties, and experimentally evaluated its performance and precision. Our results show that IES-CBIR is provably secure, allows more efficient operations than existing proposals, both in terms of time and space complexity, and enables more reliable practical application scenarios.

I. INTRODUCTION

Nowadays visual data is responsible for one of the largest shares of global Internet traffic in both corporate and personal use scenarios [1]. The amount of images, graphics, and photos being generated and shared everyday is growing at an ever increasing rate. The storage needs for such large amounts of data has been a driving factor for data outsourcing services such as the ones leveraging Cloud Storage and Computing solutions. Such services (e.g. Instagram and Flickr) have been reported to be among the largest growing internet services [2]. Additionally, the availability of large amounts of images in public and private repositories naturally leads to the need for content-based search and retrieval solutions (CBIR) [3].

Despite the fact that data outsourcing (i.e. resorting to cloud computing infrastructures) seems a natural solution to support large scale image storage and retrieval systems, it actually raises new challenges in terms of data control and privacy. This is a consequence of outsourcing data, which usually implies releasing control (and some times even full ownership) over it [4]. Recent news have provided clear proofs that privacy should not be expected to be preserved from Cloud providers [5], [6]. Furthermore, malicious system administrators working for the providers have full access to data on the hosting cloud machines [7], [8]. Finally, external hackers can exploit software vulnerabilities to gain unauthorized access to servers [9]. The recent incident with the iCloud image storage service and celebrity photo leakage [10] illustrates, in some part, the importance of these threats for cloud-based visual data stores.

The conventional approach to address privacy in this context is to encrypt sensitive data before outsourcing it and run all computations on the client side [11]. However, this imposes too much client-overhead, as data must continuously be downloaded, decrypted, processed and securely re-uploaded. Many applications cannot cope with this overhead, particularly online and mobile applications operating over very large datasets such as image repositories with CBIR services. A more viable approach would be to outsource computations and perform operations over the encrypted data on the server side. Existing proposals in this domain remain on the theoretical realm, namely those requiring fully homomorphic encryption, which are still computationally too expensive [12]. Nonetheless, partially homomorphic encryption schemes [13]–[16] and symmetric-key solutions designed for addressing specific searching problems [17]–[19] are an interesting alternative, yielding more practical results while providing a good trade-off between security (privacy) and usability. Unfortunately, even these solutions are too computationally complex for wide adoption, particularly regarding the support of privacy-preserving CBIR over large-scale, dynamically updated image repositories, and even more if we consider mobile (resource constrained) clients, which already represent the source for more than 30% of internet traffic.

To address these challenges we propose a new secure framework for the privacy-preserving outsourced storage, search, and retrieval of large-scale, dynamically updated image repositories. We base our proposal on another contribution of this work: IES-CBIR, a novel Image Encryption Scheme with Content-Based Image Retrieval properties. Key to the design of IES-CBIR is the observation that in images, color information can be separated from texture information, enabling the use of different encryption techniques with different properties for protecting each of these features. Following this observation, and considering that texture is usually more relevant than color in object recognition [20], in IES-CBIR we make the following tradeoff: we choose to privilege the protection of image contents, by encrypting texture information with probabilistic (semantically secure) encryption [21]; then we somewhat relax the security on color features, by using deterministic encryption on image color information. This methodology allows privacy-preserving CBIR based on color information to be performed directly on the outsourced servers with high security². Notably, our solution allows the outsourced servers to generate and update the resource index used to support queries, a task that in many state of the art solutions must be managed by the user devices which, as we later show in the paper, leads to excessive computational and/or communication

1 By dynamically updated we mean a repository where clients continually add, update, and remove images.
2 And shows potential for extension to many other applicational domains.
overheads with impact on performance.

This paper makes the following contributions: (i) we formally define IES-CBIR and propose an efficient construction that achieves its functionality; (ii) we show how to design an outsourced image storage, search, and retrieval framework by leveraging IES-CBIR to avoid most heavy computations (i.e., indexing of dynamically added/updated images) to be performed by the client, hence avoiding performance pitfalls that exist in previous approaches [15]–[19]; (iii) we formally prove the security of our proposed framework based on IES-CBIR; (iv) we experimentally show that when compared with competing alternatives [15], [17], our framework provides increased scalability, performance (from user’s perspective), and lower bandwidth consumption, allowing client applications to be increasingly lightweight and potentially mobile; and finally (v) we show that the retrieval precision and recall [22] of the proposed solution is on par with the current state of art.

II. RELATED WORK

Previous proposals for supporting outsourced storage, search and retrieval of images in the encrypted domain can be broadly divided in two classes: Searchable Symmetric Encryption (SSE) based approaches and Public-Key partially-Homomorphic approaches (PKHE). SSE has been widely used in the past by the research community, both for text [23]–[25] and image [17]–[19] search/retrieval. In SSE-based solutions, clients process and encrypt their data before outsourcing it to the cloud. From this processing, an index is created, encrypted, and stored in the outsourced infrastructure, which allows clients to search their data efficiently and in a secure way. Data is typically encrypted with a probabilistic symmetric-key encryption scheme, while the index is protected through a combination of probabilistic and deterministic (or even order-preserving [26]) encryption. Unfortunately, SSE-based approaches in general share the following limitations:

(i) clients either require a trusted proxy [18] or have to index their images (and encrypt that index) locally [17], which entails the use of additional computational power on their side and limits the practicality of the solution for lightweight and mobile devices. This is even more limiting if we consider dynamic application scenarios, where images are constantly being added, updated, and removed. In such dynamic cases, SSE works require multiple rounds of communication for updating image repositories and their indexes. For instance, [17] uses repository-wide statistics (inverse-document frequencies), which change as the repositories are updated and thus force re-construction and re-encryption of the index which might require clients performing such task to download and decrypt the full contents of the repository. Additionally, in [17] index values are encrypted with an order-preserving encryption scheme whose security depends on the plaintext domain distribution, and with multiple updates this distribution will change, also forcing index re-construction and re-encryption;

(ii) clients have to transfer additional data to the cloud (instead of just uploading images, they also have to retrieve and re-upload their encrypted index with each repository update). This leads to additional bandwidth usage, negatively impacting the storage operations latency as perceived by users;

(iii) as SSE works use deterministic identifiers and search trapdoors to provide their functionality with practical performance, they leak what is known as search, access, similarity, and update patterns [18], [23]–[25], which intuitively means that they reveal, respectively: if a new query has been submitted before; which images are returned by each query; which images are similar to a given query image (in case of similarity/ranked search); and which images (previously searched) are similar to a new image being inserted. As demonstrated in [27] (and even if only the search and access patterns are revealed [23]), in any long-lived system with many queries being executed and all index entries being accessed at some point in time, or when facing an adversary capable of adaptively querying the whole system [23], these leakages result in exposing as much information as a fully deterministic encryption scheme, albeit with much higher computational overhead. Nonetheless, the reader should note that deterministic schemes (and SSE-based schemes with the referred leakages) can still be provably-secure, as long as the higher-level applications leveraging them control the amount of background information leaked to adversaries [27].

The alternatives to SSE that can be found in the literature [15], [16] are based on public-key partially-homomorphic encryption (PKHE) schemes such as Paillier [13] or ElGamal [14] (which allow additions and multiplications on the encrypted domain, respectively). In these approaches, clients encrypt images pixel by pixel with a PKHE scheme, allowing the cloud to process and index their encrypted images on their behalf and thus avoiding many of the practical issues of SSE-based solutions. Unfortunately, PKHE works present much higher time and space complexities. For instance, Hsu et al. [15] proposed a high-precision CBIR algorithm in the encrypted domain, by resorting to the Paillier cryptosystem [13]. However, their approach results in significant ciphertext expansion (for a secure key size of at least 1024 bits, each pixel is transformed from its traditional 24 bits representation into 2048 ciphertext bits), slow encryption and decryption times (as we will experimentally demonstrate in our evaluation Section V-1), and in scalability issues (the “ciphertext blowup” problem [28]). Furthermore, their work was later shown to be either insecure or computationally intractable for the cloud server [29]. Zheng et al. [16] proposed a variant of that work to overcome some of its limitations, by replacing Paillier ciphertexts with pointers to a ciphertext table (built by mapping those pointers to all possible ciphertext pixel values). While this approach reduces the number of encryption operations and minimizes ciphertext expansion, it still presents a significant computational overhead which limits its practicality.

Aside from the SSE and PKHE research directions, there have been other works following similar approaches to what we propose in this paper, although for different purposes. An example is the work by Nourian et al. [30] which aims at providing privacy-preserving single image template matching performed by third-party clouds. The work doesn’t support large-scale repositories however as it only allows linear searching, requires the template being matched to be re-encrypted for comparison with each different image in a repository, and depends on the availability of public images as noise for encryption which can be easily found by an attacker using popular high-availability repositories for dictionary attacks or by tracking users’ traffic. Another example is the more theoretical work by Chase et al. [31], which propose a set of algorithms for the encryption of several data structures including matrix-based datatypes such as images, while enabling queries to be
performed over the ciphertext. However their main motivation is to extract partial information about a single encrypted data object (such as the color of a given pixel in an image) whereas we focus on allowing the generation of indices over large collections of encrypted images by an untrusted third party and the resolution of user queries over these large collections.

The reader should also note that most works on privacy-preserving image retrieval are not actually proven secure. In some works the underlying cryptographic primitives used have already been proven secure and are used as intended [17], meaning that their security correctness may be easy to infer despite the lack of a formal security analysis. However, other works rely on small modifications that can actually compromise security. Such is the case, for instance, of [15] and [30] as we discussed in the previous paragraphs, and [19] which bases its security solely on hashing functions which can be trivially compromised through dictionary attacks [21].

Table I summarizes some aspects of the previous works discussed here, by comparing our work with the most relevant approaches from SSE [17] and the PKHE [15] research contexts, in terms of information leakage and computational complexity for the clients. These works were also implemented and will be experimentally compared with a prototype of our framework in Section V. The Information Leakage column represents the leakage of all system operations (particularly the update, search, and remove operations) as a whole. The column Local Index Size represents a maximum bound on the possible index size on the clients’ side. In PKHE [15] and our work, the cloud extracts and indexes the images’ feature-vectors, however in SSE works (e.g. [17]) it’s the client who extracts image features and builds/updates the index with each repository update, so its size becomes especially relevant for the overhead imposed on clients. The final column represents the CBIR algorithms used in each work: local color histograms [17], SIFT [32], and global color histograms [33].

### III. TECHNICAL OVERVIEW

In this work we propose a framework for the privacy-preserving outsourced storage, search, and retrieval of images in large-scale, dynamically updated repositories. Our framework is composed of two main components: an image encryption component, executed on client devices; and a storage, indexing, and searching component (in the encrypted domain), executed in the outsourcing server (e.g. a cloud provider). We base this framework on a new encryption scheme specifically designed for images, called IES-CBIR. IES-CBIR allows us to design outsourced image repository systems that support content-based image retrieval (CBIR) based on color features, while protecting the privacy of both image owners and other users issuing queries. Comparing with state-of-art, IES-CBIR shows comparable retrieval precision and higher computational performance than previous approaches as perceived by the clients, since it securely moves indexing computations to the cloud provider’s infrastructure and avoids public-key and homomorphic cryptography. IES-CBIR also minimizes ciphertext expansion and consequently bandwidth and outsourced space requirements, reinforcing the positive impact on user-perceived latency. These benefits are further illustrated in our experimental analysis in Sec. V, where the performance of a IES-CBIR system is compared against the state of the art SSE [17] and PKHE [15] based approaches.

In the next subsections we present the system model for our proposed framework (Sec. III-A), followed by its adversary model and security assumptions (Sec. III-B). We also envision our models to fit well with several relevant use cases, in particular for storing Personal Health Records that include colored examinations and images (e.g. MRIs, skin cancer images), as well as for supporting the cloud storage of shared image repositories for users with mobile devices. In [34] we provide a companion technical report for this paper, where more details on the mapping between the entities of our model and these use cases are given. For the remainder of the paper we use the following terminology: a repository is a collection of images which is stored in the infrastructure of a cloud provider; the cloud server, or just cloud, is the outsourcing infrastructure that acts as a server both for storage and computation over images; users are the clients of our system, possibly using lightweight mobile devices. Each user accesses one or more repositories where they can search, add, and update images at any time; Repository keys are secret cryptographic keys that are used to search, add and update images in the repositories (each repository has its own repository key); Image keys are secret keys used for encrypting and decrypting the images in the repositories, in conjunction with the respective repository keys (each image has its own image key).

### A. System Model and Architecture

We now describe an example system model and architecture envisioned for using our framework and IES-CBIR. In this model, we consider two main entities: the cloud and (multiple) users (Fig. 1). Images are outsourced to repositories managed by the cloud. Each repository is used by multiples Users, where they can both add their own images and/or search using a query image. Users can also request access to stored images from their creators/owners. Our objective is to ensure the privacy of users, hence all data sent to the cloud is encrypted.
Repositories are created by a single user. Upon the creation of a repository, a new repository key is generated by that user and then shared with other trusted users, allowing them to search on the repository and store new images. To add/update images, a user further needs an image key (locally) generated for that image. Image keys are kept secret by their users, meaning that even users capable of searching in a repository (i.e., with access to the repository key) will need to ask the owners of specific images for access to them. Note that using specific keys per-image should be seen as optional in our framework, i.e. if the users of a repository prefer to avoid further key management work and are willing to sacrifice fine-grained access control, they can use the same image key for all images or in groups of images.

When the cloud receives an encrypted image for storage it extracts its relevant features (in our framework, we use global color features [33]) and indexes the image based on these features. The same action is performed for a query image, which after being encrypted by a user with a repository key, is then processed by the cloud and have its features extracted and matched with the repository’s index. The reply to a query will contain a (configurable) $k$ number of encrypted images and respective metadata, which include each image’s id and the id of the user that owns each of the images. To fully decrypt and access the contents of an image, besides the repository key, the querying user will further require the image key for that specific image.

It should be noted that all key sharing interactions can be done asynchronously and out-of-band, by resorting to a trusted key-sharing protocol with public-key authentication such as Needham-Schroeder-Lowe [21]. User authorization and revocation can also be easily achieved through the sharing (and refreshment when user revocations are issued) of repository-specific tokens between trusted users, and its request in the framework operations. Nonetheless, we find these discussions to be orthogonal to the main focus of this paper, as the mechanisms involved can be easily integrated into our framework.

B. Adversary Model and Assumptions

In this work we aim at protecting the privacy of users’ images and queries. The main adversary we consider is the malicious cloud administrator, who operates the cloud’s infrastructure and servers. Similar to many previous works found in the literature [17], [18], [23]–[26], we assume an honest-but-curious cloud model [4], that is, the cloud is seen as a passive adversary that is expected to correctly perform operations when asked (i.e., fulfill its contract agreements), but may eavesdrop on users’ data. We assume that a malicious cloud administrator has access to all data stored on disk or in RAM on any device physically located at the cloud, and passing through the network from or to the cloud. In Section IV-C, we formally prove the security of our framework against such an adversary.

A stronger adversary that should also be considered in this work is a malicious user, i.e. a user of the system who deviates from his expected behavior. Malicious users are an open problem for any multi-user application, as they may be given access to multiple repository and image keys before being discovered, and can more easily eavesdrop on other users’ images. In this work we focus on protecting our proposals and proving their security against the malicious cloud administrator, and leaving the malicious users issue as an open and interesting future research direction. Nonetheless, we acknowledge that different orthogonal mechanisms can be deployed to mitigate the challenges introduced by malicious users, including access control techniques, repository access revocation and periodic key refreshment. We also assume that distinct adversaries (i.e. a malicious user and the cloud administrator) can collude with each other, as they will not gain any further advantage as a whole against the system. Furthermore, we don’t consider integrity or availability threats, as they can be handled by different mechanisms orthogonal to the contributions of this paper [35]–[37]. Finally, we assume that the higher-level applications using our framework control the amount of background information leaked, as this information may be sensitive and can be leveraged by adversaries for breaking security.

IV. A PRIVACY-PRESERVING CBIR FRAMEWORK

In this section we present the design and details of our proposed framework. We start by formally defining IES-CBIR and its algorithms (Sec. IV-A). Then we explain how the framework’s component in the cloud server side leverages IES-CBIR properties to store, index and search images while preserving their privacy (Sec. IV-B). Finally we detail the system protocols of our framework and formally prove its security (Sec. IV-C).

A. IES-CBIR Design and Implementation

The main component on the users’ side leverages a novel cryptographic scheme specifically designed for images and privacy preserving CBIR, dubbed IES-CBIR. Before describing IES-CBIR in detail, we give a definition of image privacy underlines our work.

Informally, we define image privacy as the ability to keep the contents of an image secret to public (or simply unauthorized) disclosure [38]. Generally speaking, image contents are characterized by the combination of its color and texture information. These two components form what one can readily identify in an image: objects, people, etc. As such, to safeguard image privacy entails preventing unauthorized entities from recognizing objects in those images. We further remark that image color and texture informations can be separated from each other. In fact, color information is given from pixel color
values in the different channels of some color models; while texture information is given by the (relative) position of pixels and strong color changes across neighboring pixels. We also remark that texture information is usually more relevant in images for object recognition [20]. Finally, we conclude that no sub-component alone (i.e. color or texture information) can be used to infer the precise contents of an image, as color information on itself is usually ambiguous (e.g. strong blue can translate into sky, ocean, etc.) and texture information depends not only on pixel positions but also on their color values. These conclusions are further supported by the most recent works in image reconstruction [39], which not only depend on local features extracted from sub-parts of the images (in this work we focus on global features extracted from each image as a whole), but also on those local features not being encrypted.

Leveraging the previous definition and observations, we design IES-CBIR, an image encryption scheme that separates color from texture information, applying different encryption techniques for protecting each: emphasizing that texture is usually more relevant than color for object recognition [20], we design IES-CBIR to protect image texture with probabilistic encryption and color information with deterministic encryption. This way, content-based image indexing and retrieval, based on color information, can be performed on the cloud servers in a privacy-preserving way and without intervention of users, while texture information remains protected with the highest level of security (we provide a detailed and formal security evaluation in Sec. IV-C). We define IES-CBIR as:

**Definition 1 (IES-CBIR).** An Image Encryption Scheme with CBIR properties (IES-CBIR) is a tuple (GENRK, GENIK, ENC, DEC, TRPGEN) of five polynomial-time algorithms run by a user, where:

- **GENRK**(sp): is a probabilistic algorithm that takes as input the security parameter sp ∈ N and generates a repository key rk with length polynomially bounded by sp;
- **GENIK**(sp): is a probabilistic algorithm that takes as input the security parameter sp ∈ N and generates an image key ik with length polynomially bounded by sp;
- **ENC**(I, rk, ik): is an algorithm that takes as input an image I and the cryptographic keys {rk, ik} and returns an encrypted image C1;
- **DEC**(C1, rk, ik): is an algorithm that takes as input an encrypted image C1 and keys {rk, ik} and returns the decrypted image I1;
- **TRPGEN**(Q, rk): is an algorithm that takes as input a query image Q and a repository key rk and returns a searching trapdoor CQ.

1) **Key Generation:** As already discussed in our system model (Sec. III-A), IES-CBIR works with two different types of cryptographic keys, repository keys (rk) and image keys (ik), which are generated by the GENRK and GENIK algorithms respectively. In our design and implementation of IES-CBIR, we specify that repository keys are generated by making three independent random permutations of all values in the range [0..100]. These permutations can be generated through a Pseudo-Random Generator (PRG) [21] G, parameterized with some random seed (in our implementation we instantiate G with an AES-based PRG [21]). This results in 3 subkeys: rk_H, rk_S, rk_V (Eq. 1). The range [0..100] represents all possible color values in the HSV color space ((H) hue, (S) saturation, (V) value/brightness), and each different subkey is attributed to a color channel. We choose to maintain the same domain of possible values with encryption in order to reduce ciphertext expansion and to allow image processing operations to be done “as is”, including CBIR, indexing and image compression/decompression. Therefore, key \( rk = \{ r_{k_H}, r_{k_S}, r_{k_V} \} \) enables deterministic encryption of color information by (pseudo)randomly permuting all pixel color values in the three HSV color channels\(^3\). In this case, \( sp_{ik} \) takes the value 303 \( \times \) 8 = 2424 bits.

\[ rk_H, r_{k_S}, r_{k_V} \leftarrow \text{RandPerm}(G, [0..100]), \; rk = \{ r_{k_H}, r_{k_S}, r_{k_V} \} \]  

(1)

In contrast, key ik is generated by requesting 128 (the \( sp_{ik} \)) pseudorandom bits to \( G \). ik will be used as a cryptographic seed for the probabilistic encryption counterpart of IES-CBIR.

2) **Encryption:** Image encryption in IES-CBIR is achieved through two main steps and a final (optional) step: \( i) \) pixel color values encryption, \( ii) \) pixel positions permutation, and \( iii) \) image compression. The goal of the first step is to protect image color features, through the application of a Pseudo-Random Permutation (PRP) [21] P on all pixel color values. Although we could use a standard PRP construction to instantiate \( P \) (such as an AES-based PRP [21]), we chose to conceive a specific color-domain PRP, allowing us to preserve the format of encrypted images. Our construction encrypts pixel color values by deterministically replacing them, in each color channel, using repository key \( rk = \{ r_{k_H}, r_{k_S}, r_{k_V} \} \). Eq. 2 represents this operation, where \( P_{rk}(p_x) \) is the encryption of pixel \( p \)'s value in color component \( x \) through \( P \) and key \( rk_x \).

\[ C_I \leftarrow P_{rk_x}(p_x) : \forall x \in \{H, S, V\}, \forall p \in I \]  

(2)

This step of encryption securely hides the color values of the encrypted pixels. However, due to the deterministic properties of \( P \) (a requirement to enable CBIR in the encrypted domain), patterns present in the original image (which denote its texture) will remain visible. To fully protect image contents, we rely on a second probabilistic step in our encryption algorithm: (pseudo)random pixel position permutation, through pixel rows and columns shifting. This step consists in the following: a PRG \( G \) is instantiated with a previously generated image key \( ik \) (operation GENIK above) as cryptographic seed. Then, for each pixel column, we request from \( G \) a new pseudorandom value \( r \) between 1 and the image height, and do a downward shift on that column of \( r \) positions, overflowing to its beginning. After all columns have been randomly shifted, we repeat the procedure for the rows (with random values ranging between 1 and the image width). Eqs. 3 and 4 formally describe this step, where \( w \) and \( h \) are, respectively, the width and height of image \( I \). Note that this encryption algorithm has no ciphertext expansion (i.e. after encryption the image has the same width and height as before).

\[ C_I(x, y) \leftarrow C_I(x, (y + r) \mod h) : \forall x \in \{1, \ldots, w\}, \forall y \in \{1, \ldots, h\} \]  

(3)

\[ C_I(x, y) \leftarrow C_I((x + r) \mod w, y) : \forall x \in \{1, \ldots, w\}, \forall y \in \{1, \ldots, h\} \]  

(4)

This second step is probabilistic, as each new image will have a new pseudorandomly generated \( ik \), even if the same image is

\(^3\)Instead of encrypting pixel color values with deterministic encryption, we could also use Order-Preserving Encryption [26], slightly increasing image retrieval precision at the expense of greater information leakage.
stored multiple times with different names (if the same image key is used for all images, then a random \( iv \) must also be used as input to \( \mathcal{G} \)). Moreover, this step effectively hides existing texture patterns in the image, making it computationally unfeasible to extrapolate correlations between the plaintext and ciphertext. We choose to shift rows and columns, instead of pseudorandomly permuting all single pixel positions, because its more efficient (only \( w + h \) pseudorandom values are required instead of \( w \times h \)) and we obtain similar robustness against cryptanalysis even for images as small as \( 10 \times 16 \) pixels (see security analysis in Sec. IV-C).

The final, optional step in our encryption algorithm is to perform image compression. This is possible due to the format-preserving properties of IES-CBIR, and can be achieved through the use of a non-lossy image compression scheme such as PNG, directly over the encrypted image (additionally one can use more generic file compression algorithms such as ZIP or RAR). This step allows to control a tradeoff between computational requirements and encryption time with that of network traffic and cloud storage requirements.

3) Decryption: The decryption algorithm applies the different steps of encryption in the opposing order, or more formally, through the ordered application of the transformations denoted by Eqs. 5, 6, and 7 (after decompressing the ciphertext if required). Note that the \( r \) random values must be generated in the same order as in the encryption.

\[
C_I(x + r) \mod w, y) \leftarrow C_I(x, y) \forall x \in \{1, \ldots, w\}, \forall y \in \{1, \ldots, h\} \tag{5}
\]

\[
C_I(x, (y + r) \mod h) \leftarrow C_I(x, y) \forall x \in \{1, \ldots, w\}, \forall y \in \{1, \ldots, h\} \tag{6}
\]

\[I \leftarrow P_{rk}(c_{pk}) : \forall x \in (H, S, V), \forall c_{pk} \in C_I \tag{7}
\]

4) Searching-Trapdoor Generation: The TrpGen algorithm generates searching trapdoors that users can leverage to search over image repositories. Trapdoor generation requires a query image \( Q \) as input, as well as the repository key \( rk \). This means that users with access to \( rk \) will be able to access color values of all images stored in that repository. However, users can’t access texture information (and hence full image contents) without the corresponding image keys, and can’t use \( rk \) to search other repositories. Given \( rk \), the TrpGen algorithm operates in a similar fashion to the ENC algorithm (Eq. 8, where the image key is substituted by a new randomly generated \( ik \)). This means that searching trapdoors are also decryptable, and can be stored in the repositories as new images as long as the querying users locally save the generated image keys.

\[Trp(Q, rk) \leftarrow Enc(Q, rk, ik) \tag{8}\]

B. CBIR in the Encrypted Domain

On the cloud’s side, the received encrypted images are processed and indexed for CBIR before being persistently stored. IES-CBIR enables these operations (for color features) to be performed over their ciphertexts, using algorithms that operate on non-encrypted images and without requiring any modifications. Encrypted image processing has two main steps: feature extraction and feature indexing. Feature extraction consists in processing an image and extracting a reduced set of feature vectors that describe it. In this work we focus on color features in the HSV color model and their representation as color histograms. For each encrypted image and each HSV color channel, the cloud server builds a color histogram by counting the number of pixels in each intensity level. This yields 3 color histograms with 101 entries each.

Upon extracting these features, the cloud can perform feature indexing to speedup query execution. In this work, we use the Bag-Of-Visual-Words (BOVW) representation [40] to build a vocabulary tree and an inverted list index for each repository. We choose this approach for indexing as it shows good search performance and scalability properties. In the BOVW model, feature-­vectors are hierarchically clustered (for instance, using the \( k \)-means algorithm [40]) into a vocabulary tree (also known as codebook), where each node denotes a representative feature-­vector in the collection and leaf nodes are selected as the most representative nodes (called visual words). This clustering step requires a training dataset, so in the prototype implementation of our framework based on IES-CBIR, we request an initial image collection from users when creating a new repository. After the creation of the codebook, additional images can be stored dynamically by hierarchically stemming them against it. This stemming returns the closest visual words to the image, according to some distance function (in our prototype we use the Hamming/L1 Distance). Finally, the cloud server builds an inverted list index, with all visual words as keys and, as values, the list of images (and a frequency score for the visual word in the image) most close to them. This type of list is known as a Posting List [3].

After processing and indexing encrypted images, the cloud server can receive search requests from users, through the submission of searching trapdoors for some query images of their choice. When a new searching trapdoor is received, the cloud server extracts its color feature-­vectors and finds their closest visual words by stemming them against the codebook. The query’s visual words are used to access the repository’s index, obtaining the corresponding posting lists in the process. Then, for each image referenced in at least one posting list, a search score is calculated for that image (in our implementation we use a “scaled tf-­idf” scoring function [17]). Finally, the cloud server returns the top \( k \) images to the user, according to their scores \( (k \) is a configurable parameter). The BOVW approach guarantees that only the most relevant images (a fraction of the repository) have to be compared in the scoring step (ensuring scalability). After receiving these ranked results, users can explicitly request full access to images by requesting the corresponding image keys from their owners.

C. Framework Protocols and Security Analysis

We start this sub-­section by providing an idealized functionality for our framework. Then we present the details of our IES-CBIR based framework construction and formally prove it securely materializes the idealized functionality. Our security proofs follow the real/ideal paradigm that is standard in secure multi-­party computations [41].

Algorithm 1 formalizes the ideal functionality \( F \) of our framework. In \( F \) we consider as adversary the honest-­but-­curious cloud provider (Section III-­B), which corrupts the cloud server passively. As stated in Section II, the leakage functions specified in Alg. 1 are equivalent to the search, access, similarity and update leakages of SSE-­based works [18], [23–25], particularly for any long-­lived system with many
**Algorithm 1** The ideal functionality of our framework, $F$; all information leaked is specified here.

$F$ is specified as a trusted third-party, which mediates inputs and outputs between a user and the cloud server, modeling all information leaked to the later. $F$ accepts four commands, with inputs identical to the commands of the cloud server:

- **CreateRepository** ($ID_R, \{ID_{ID_1, I}\}_{i=0}^{\infty}$) - Upon receiving this command from the user identified by $ID_U$:
  - $F$ initializes a new repository $Rep_R$ and creates a new index $Idx_R$ with size $n$. Then $F$ stores and indexes the initial set of images $\{ID_{ID_1, I}\}_{i=0}^{\infty}$, creating in the process the clustering codebook $CB_k$ with height $m$ and leaf width $n$.
  - **Setup Leakage** $F$ sends to the cloud server the deterministic identifiers of the repository ($ID_R$), of the user creating it ($ID_U$) and of each initial image ($ID_{ID_1}$). Additionally, $F$ sends initialization parameters $n$ and $m$ and, for each initial image $I$, $F$ sends its width in pixels ($w_I$), its height ($h_I$), and deterministic identifiers of the visual words contained in $I$ and their frequency ($\{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty}$).

- **StoreImage** ($ID_R, ID_{ID_1, I}, ID_U$) - If $R$ doesn’t exist, $F$ returns an error. Otherwise:
  - $F$ persists stores image $I$ in $Rep_R$ and indexes it, updating $Idx_R$ in the process.
  - **Storage Leakage** $F$ sends to the server $ID_R, ID_{ID_1, I}, ID_U, w_I, h_I$ and $\{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty}$.

- **Search** ($ID_R, ID_{ID_1, I}, ID_U$) - $F$ processes query image $Q$ and returns the most relevant image results in descending order, according to $Idx_R$.

- **Remove** ($ID_R, ID_{ID_1}$) - If $R$ doesn’t exist or $I$ isn’t an image of $R$, $F$ returns an error. Otherwise:
  - $F$ removes the image identified by $ID_{ID_1}$ from $Rep_R$ and from $Idx_R$.
  - **Remove Leakage** $F$ sends to the server $ID_R$ and $ID_{ID_1}$.

queries being executed as expected from real-world application scenarios. Furthermore, applications using our framework can ensure that the information leaked will not compromise their security, by limiting the amount of background information made available to an adversary [27]. In algorithms 2, 3, and 4 we detail the protocols of our IES-CBIR based framework’s construction: respectively the Create Repository, Store Image and Search protocols (the protocols for the Remove and Access Image operations are straightforward and can be found in the companion technical report [34]). In these protocols we omit operations related with the request and sharing of keys, as these are orthogonal to the scope of the paper.

The proof that our framework’s construction securely realizes $F$ involves showing that a simulator $\mathcal{S}$, interacting with a user only through $F$ (the ideal experiment), can simulate the view of the cloud server in a real interaction with the user through an instance of our construction (the real experiment), and that the two experiments would be indistinguishable (apart from a negligible probability), even when combined with the adaptively influenced inputs of the client. The essential rational that justifies our security properties is as follows: In the ideal functionality $F$, when the user stores an image or sends it as query to a repository, the server basically learns its similarity to the images stored there, based on a distance function over their color histograms, and nothing more. In the real experiment, the user will invoke (through our construction’s protocols) the algorithms of IES-CBIR to achieve the same functionality. Thus, the crucial point in proving security is to show that IES-CBIR leaks no additional information to the server.

Formally, a simulator can simulate the view of the adversary randomly, based only on the size (number of images) of the repository. The only difference between this simulation and the real execution is the following: in the real execution there is a limitation on the size (in terms of pixel width and height) of the images being stored and searched. In fact, IES-CBIR algorithms can only be proven computationally secure for images with at least $16 \times 16$ pixels of width and height, respectively. For images smaller than that, a Probabilistic Polynomial-Time (PPT) bounded adversary can compromise the probabilistic counterpart of IES-CBIR encryption in useless time. In the simulation, such limitation does not exist. As such, the proof must show that if this requirement on the size of images is respected by the user, security properties will hold and the real and ideal experiments will be indistinguishable.

**Theorem 1.** Our framework’s construction based on IES-CBIR securely realizes $F$ against honest-but-curious PPT

**Algorithm 2** Create New Repository

1: procedure USER($ID_U$) \text{CREATEREPOSITORY}($ID_R, sp_{vk}, sp_{sk}, n, m$, $\{ID_{ID_1, I}\}_{i=0}^{\infty}$)
2:     $rk_{R} \leftarrow$ IES-CBIR.GenRK($sp_{vk}$)
3:     for all $\{ID_{ID_1, I}\}_{i=0}^{\infty}$ do
4:         $ik_{D_{ID_1, I}} \leftarrow$ IES-CBIR.GenIK($sp_{sk}$)
5:         $C_{D_{ID_1, I}} \leftarrow$ IES-CBIR.Enc($ID_{ID_1, I}, rk_{R}, ik_{D_{ID_1, I}}$)
6:     end for
7:     $LOUD.CREPOSITORY(ID_R, n, m, ID_U, \{ID_{ID_1, C_{ID_1}}\}_{i=0}^{\infty}$)
8:     return $(rk_{R}, \{ik_{D_{ID_1, I}}\}_{i=0}^{\infty}$)
9: end procedure

10: procedure $LOUD.CREPOSITORY(ID_R, n, m, ID_U, \{ID_{ID_1, C_{ID_1}}\}_{i=0}^{\infty}$)
11:     $Rep_R \leftarrow \{ID_{ID_1, C_{ID_1}}\}_{i=0}^{\infty}$ - InitializeRepository()
12:     $Idx_R = \{ID_{vw_1}, \{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty} \}_{i=0}^{\infty} \leftarrow$ InitializeIndex($n$)
13:     for all $\{C_{ID_1, i}\}_{i=0}^{\infty}$ do
14:         $func_{C_{ID_1, i}} \leftarrow \{\text{hist}_{F}, \text{hist}_{S}, \text{hist}_{V}\} \leftarrow$ ExtractFeatures($C_{ID_1, i}$)
15:     end for
16:     $CB_R \leftarrow$ ClusterFeaturesIntoCodebook($n, m, \{func_{C_{ID_1, i}}\}_{i=0}^{\infty}$)
17:     for all $\{ID_{ID_1, C_{ID_1, i}}\}_{i=0}^{\infty}$ do
18:         $func_{C_{ID_1, i}} \leftarrow \{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty} \leftarrow$ CB.R Stem($func_{C_{ID_1, i}}$)
19:             for all $\{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty}$ do
20:                 $Idx_R[\{ID_{vw_1}, \text{freq}_{ID_{vw_1}}\}_{j=0}^{\infty}] \leftarrow$ CB.R Stem($func_{C_{ID_1, i}}$)
21:     end for
22:     $Rep_R[ID_{ID_1}] \leftarrow \{C_{ID_1, i}, ID_U\}$
23:     end for
24: end procedure
Algorithm 3 Store/Update Image

1: procedure User(ID$_R$).UpdateImage(ID$_R$, rk$_R$, ID$_I$, I, sp$_{ak}$)
2:   \( i_kI \leftarrow\) IES-CBIR.GenIK(sp$_{ak}$)
3:   C$_I \leftarrow\) IES-CBIR.Enc(I, rk$_R$, i_kI)
4: end procedure

Algorithm 4 Search with an Image as Query

1: procedure User(ID$_U$).Search(ID$_R$, Q, rk$_R$, k)
2:   C$_Q \leftarrow\) IES-CBIR.GenTrQP(Q, rk$_R$)
3:   rankedImgDistances \leftarrow\) cloud.Search(ID$_R$, C$_Q$, k)
4: end procedure

adversaries, provided that all images used as input have at least 16x16 pixels of width and height, respectively.

The full proof of this theorem can be found in our companion technical report [34]. Nonetheless we provide here the main argument for the previous limit on images’ size. Consider a distinguisher D, executed by S to distinguish the output of the real experiment (image I) from the output of the simulation (simulated image I'). D’s computational complexity in distinguishing I from I' is shown in [34] to be \( w^w \times h^h \) (due to the pseudorandom permutation of pixel rows and columns). If we consider 128 as minimum security bound for sp$_{ak}$ (as recommended for AES encryption [21]), then \( w^w \times h^h \) should be at least \( 2^{128} \). Since an image of 16x16 pixels of width and height leads to \( 16^{16} \times 16^{16} = 2^{128} \), this represents the minimum security bound for ensuring that I is computationally indistinguishable from I'.

V. EXPERIMENTAL EVALUATION

In this section we experimentally evaluate our proposals and compare them with some of the most relevant competing alternatives. To this end we have implemented, in the Java language, a prototype of our IES-CBIR based framework (as described in Sections IV-A and IV-C) and prototypes of the competing relevant works: i) the SSE solution proposed in [17], based on Bag of Visual Words indexing and Order-Preserving Encryption (labelled SSE in the graphics presented in this section); and ii) a system leveraging the Paillier cryptosystem described in [15] (labelled PKHE). Leveraging these prototypes, we conducted an experimental evaluation of the performance and precision of our solution and the competing works. All experimental assessments were carried out using Amazon EC2 instances, both for user simulation and for running the cloud storage and computation component. To simulate geographic distance, user processes were executed in Oregon’s data-center instances, while the cloud component was deployed in a North-Virginia’s data-center instance. User instances, in our framework’s testing scenario, were of the general-purpose m3.medium type and the cloud server was of the m3.large type. In the competing works testing scenarios user instances had to be increased to the m3.large type, as they have to perform heavier computations. For testing purposes, we used two image datasets: the Wang dataset [20], containing 1000 low-resolution images with a JPEG compressed size of 29.8 MB; and the Inria Holidays Dataset [42], containing 1491 high-resolution images with total JPEG compressed size of 2.85 GB. Figure 2 shows an example of an image from the Holidays Dataset and its IES-CBIR encryption. We present our results in the following order: first we discuss the performance and scalability of our solution, comparing it with the alternative approaches; then we study the achieved retrieval precision.

1) Performance: In these experiments we used the larger sized Holidays dataset to compare the performance of our system, with and without image compression (labeled IES-CBIR w/ compression and IES-CBIR no compression respectively) with that the competing alternatives SSE and PKHE. To this end we have measured the time taken by the Update Image operation with two distinct workloads: one where the 1491 (2.85 GB) images from the Holidays Dataset are used to create and populate a new image repository in the cloud, and another where after the initial upload of 1491 images, another 150 users try to upload 10 new images each concurrently (total 5,68 GB). This last workload allow us to show hidden overheads of updating repositories in some alternatives described in the literature, especially when multiple users try to store new images concurrently. Fig. 3 summarizes the results for each system, in terms of time required for each sub-operation (Encryption, Indexing, Training (i.e. the hierarchical k-means clustering necessary once for each repository, as described in

\[http://aws.amazon.com/ec2/instance-types/\]
The results show that IES-CBIR with image compression offers overall better performance when compared with the remaining competing alternatives. This is a consequence of the very high cryptographic throughput presented by IES-CBIR, combined with the fact that users only have to encrypt their images. In contrast, other alternatives either present very slow cryptographic throughput (PKHE), or additionally require indexing operations from the users (SSE). In more detail: IES-CBIR without compression presents slightly higher cryptographic throughput, but the performance gained there is somehow lost when the user has to upload larger decompressed images; PKHE shows prohibitive overheads both due to the low cryptographic throughput of the public-key Paillier cryptosystem and to its high ciphertext expansion (which then has to be uploaded to the cloud server); and SSE requires expensive initial training performed by the creating user for each new repository, in order to build the clustering codebook required for indexing, and then also requires the user to index locally his images.

An argument that could be made in favor of the SSE approach is that the initial training only has to be performed once, and its cost is amortized in the long run. However our second workload, where multiple users try to add additional images to the repository, shows that is not the case. In this second workload our solution (with compression) is still the one that offers overall best performance and scalability, showing an overall time increase of 9% compared to 83% for SSE (if we discard its training/clustering time) and 8% for PKHE. The SSE increase is mostly due to users having to retrieve the repository’s index, decrypt it, update its entries, encrypt and re-upload it to the cloud server, for each repository update (or bulk of updates). Moreover, this has to be done synchronously between users, to guarantee that the repository index remains in a consistent and correct state. The PKHE approach shows the same performance degradation as IES-CBIR, which is still prohibitively slow for practical adoption, and IES-CBIR without compression is still slightly slower than its compressed counterpart. The detailed results for the SEARCH w/ QUERY IMAGE OPERATION can be found in the companion technical report, nonetheless we summarize that even for searching IES-CBIR shows better performance than SSE and PKHE (mainly due to cryptographic overheads in the competing alternatives).

2) Retrieval Precision and Recall: We start by defining the metrics used herein [22]: when a search is done, precision is the number of relevant images retrieved across all returned results; recall is the number of relevant images retrieved from all the relevant results for the query; average precision (AP) is the average of the precision measured each time a new relevant image is retrieved; and mean average precision (mAP) is the mean of APs for a group of queries.

To evaluate the retrieval precision that can be achieved with IES-CBIR, we extracted two metrics: an interpolated recall-precision graph, built with the Wang dataset and all its images as queries; and the mAP of the Holidays dataset, for a group of queries pre-defined by the authors of the dataset [42]. Regarding the first experiment, we used a workload where each image in the dataset is used as query over all others in the repository. We then computed the average precision and recall, for all possible response sizes (\([1, \ldots, 1000]\)). Similar to the previous section, we compared the precision of IES-CBIR with it’s competing alternatives, SSE and PKHE. We also assessed the precision that an adversary would achieve if he was to search in the repository with a randomly chosen repository key. Figure 4 summarizes the results. Our framework shows similar precision and recall as the compared alternatives, with a small variation of about 6% in precision compared to SSE and PKHE systems. This small difference is the advantage gained by these alternatives through the sacrifice of performance and scalability. Nonetheless, the reader should note that our approach can be extended to also consider texture information in its CBIR algorithm, increasing retrieval precision at the expense of increased information leakage. Regarding the IES-CBIR with wrong key baseline, results show that a malicious user using the framework to search repositories with an incorrect repository key would achieve similar precision as if he was choosing random images from those repositories as answer.

The second precision test we performed consisted in using the evaluation package of the Holidays dataset (available online [42]) for calculating the mAP of a group of 500 pre-defined queries. Table II shows the results. In this experiment, PKHE achieved the best result, as expected due to the use of the SIFT retrieval algorithm [32], and IES-CBIR achieved the second highest results, followed by SSE. Comparing to the results of the previous experiment, we conclude that in some datasets IES-CBIR can actually achieve better precision than some of the competing alternatives, including personal photos and holidays datasets as is the of the Inria dataset [42]. Furthermore, based on all the results presented in this section, we conclude that a framework leveraging IES-CBIR achieves a good trade-off between precision/recall and performance/scalability.
In this paper we have proposed a new secure framework for the privacy-preserving outsourced storage, search, and retrieval of large-scale, dynamically updated image repositories, where the reduction of client overheads was a central aspect. In the basis of our framework is a novel cryptographic scheme, specifically designed for images, named IES-CBIR. Key to its design was the observation that in images, color information can be separated from texture information, enabling the use of different encryption techniques with different properties for each one and allowing privacy-preserving Content-Based Image Retrieval to be performed by third-party, untrusted cloud servers. We formally analyzed the security of our proposals, and additional experimental evaluation of implemented prototypes shows that our approach achieves an interesting trade-off between precision and recall in CBIR, while exhibiting high performance and scalability when compared with alternative solutions. As future work we plan to explicitly address orthogonal issues in our design, such as key sharing, user access control, and reliability issues. We also plan to investigate the applicability of our methodology – i.e., the separation of information contexts when processing data (color and texture in this paper) – in other domains beyond image data.

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VI. Conclusions

| IES-CBIR | SSE | PKHE |
|----------|-----|------|
| mAP (%)  |     |      |
| 54.564   | 49.075 | 57.9 |

TABLE II: Mean Average Precision (mAP) for the holidays dataset

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