Study of $B \to D^{(*)}\overline{D}^{(*)}$ decays with the BABAR detector

The BABAR Collaboration

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Abstract

Decays of the type $B \to D^{(*)}\overline{D}^{(*)}$ can be used to provide a measurement of the parameter $\sin 2\beta$ of the Unitarity Triangle that is complementary to that derived from the mode $B^0 \to J/\psi K_S^0$. Here we report a measurement of the branching fraction and a study of the $CP$ parity content for the decay $B^0 \to D^{*+}D^{*-}$ with the BABAR detector. With data corresponding to an integrated luminosity of 20.7 fb$^{-1}$ collected at the $\Upsilon(4S)$ resonance during 1999-2000, we determine the branching fraction to be $B(B^0 \to D^{*+}D^{*-}) = (8.0 \pm 1.6(stat) \pm 1.2(syst)) \times 10^{-4}$. The measured fraction of the component with odd $CP$ parity is $0.22 \pm 0.18(stat) \pm 0.03(syst)$. Observation of a significant number of candidates in the decay modes $B^0 \to D^{*+}D^-$ and $B^+ \to D^{*+}D^{*0}$ is reported. All results presented in this note are preliminary.

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1 Introduction

One of the most important goals of the \textit{BABAR} experiment is to precisely measure the angles of the Unitarity Triangle. While the decay $B^0 \to J/\psi K_S^0$ can be used to measure $\sin 2\beta$, the Standard Model predicts that the time-dependent CP-violating asymmetries in the decays $B^0 \to D^{(*)+} D^{(*)-}$ can also be used to measure the same quantity \cite{1}. An independent measurement of $\sin 2\beta$ in $B^0 \to D^{(*)+} D^{(*)-}$ modes is especially important since several typical extensions to the Standard Model can lead to different asymmetries between this quantity in $B^0 \to D^{(*)+} D^{(*)-}$ events and charmonium events \cite{2}. Measurements of $\sin 2\beta$ in $B^0 \to D^{(*)+} D^{(*)-}$ would thus provide stringent tests of CP-violation in the Standard Model and have significant potential to indicate deviations from it. However, the vector-vector decay $B^0 \to D^{(*)+} D^{(*)-}$ is not a pure CP eigenstate and a sizeable dilution of the measured asymmetry can be produced by a non-negligible $P$-wave CP-odd component. The dilution can, in principle, be completely removed by a time-dependent angular analysis of the decay products \cite{3}.

The rate for the Cabibbo-suppressed decays $B \to D^{(*)} \overline{D}^{(*)}$ can be estimated from the measured rate of the Cabibbo-favored decays $B \to D^{(*)}_{s} \overline{D}^{(*)}$:

$$\mathcal{B}(B \to D^{(*)} \overline{D}^{(*)}) \approx \left( \frac{f_D^{(*)}}{f_{D^s}^{(*)}} \right) \tan^2 \theta_C \cdot \mathcal{B}(B \to D^s_{s} \overline{D}^{(*)}),$$

(1)

where $\theta_C$ is the Cabibbo angle, and $f_{D^{(*)}}$ and $f_{D^s}$ are decay constants. From this it follows that the $B \to D^{(*)} \overline{D}^{(*)}$ branching fractions are of the order of $10^{-3}$. Previous measurements of branching fractions and upper limits for these modes are summarized in Table 1.

In section 2 we describe briefly the \textit{BABAR} detector and the dataset. Section 3 describes the measurement of the branching fraction $B^0 \to D^{(*)+} D^{(*)-}$ and section 4 the corresponding angular analysis to extract the CP-even component of the decay. Finally, in section 5 we discuss the observation of the decays $B^0 \to D^{(*)+} D^{(*)-}$ and $B^+ \to D^{(*)+} D^{(*)0}$. Section 6 summarizes our results.

Table 1: Summary of branching fraction and upper limit measurements performed by the CLEO \cite{4} and ALEPH \cite{5} experiments. Upper limits are quoted at the 90\% confidence level.

| Decay                  | Branching Fraction (x10^-4) |
|------------------------|-----------------------------|
| $B^0 \to D^{(*)+} D^{(*)-}$ | 9.9^{+4.2}_{-3.3} (stat) ± 1.2 (syst) |
| $B^0 \to D^{(*)+} D^-$   | $< 6.3$                     |
| $B^+ \to D^{(*)+} D^{(*)0}$ | $< 110$                  |

2 The \textit{BABAR} detector and dataset

The data used in this analysis were collected with the \textit{BABAR} detector \cite{6} at the PEP-II storage ring \cite{7} located at the Stanford Linear Accelerator Center. This data sample represents an integrated luminosity of 23.3 fb$^{-1}$, with 20.7 fb$^{-1}$ collected on the $\Upsilon(4S)$ resonance. The total number of $B \overline{B}$ pairs produced in this sample was $N_{B \overline{B}} = (22.7 \pm 0.36) \times 10^6$.

Charged particles are detected and their momenta measured with the combination of a 40-layer drift chamber (DCH) and a five-layer silicon vertex tracker (SVT) embedded in a 1.5 T solenoidal...
magnetic field. Photons are detected by a CsI electromagnetic calorimeter (EMC) that provides excellent angular and energy resolutions with a high efficiency for energies above 20 MeV. Charged particle identification is provided by the specific ionization loss ($dE/dx$) in the tracking devices and by an internally reflecting ring-imaging Cherenkov detector (DIRC) covering the barrel region of the detector.

3 Measurement of the $B^0 \rightarrow D^{*+}D^{*-}$ branching Fraction

$B^0$ mesons are exclusively reconstructed by combining two charged $D^*$ candidates reconstructed in a number of $D^*$ and $D$ decay modes. Events are pre-selected by requiring that there be three or more charged tracks and that the normalized second Fox-Wolfram moment of the event be less than 0.6. We also require that the cosine of the angle between the reconstructed $B$ direction and the thrust axis of the rest of the event be less than 0.9.

Charged kaon candidates are required to be inconsistent with the pion hypothesis, as inferred from the Cherenkov angle measured by the DIRC and the specific ionization measured by the SVT and DCH. No particle identification requirements are made for the kaon from the decay $B^0 \rightarrow K^-\pi^+$. 

$K^0_s \rightarrow \pi^+\pi^-$ candidates are required to have an invariant mass within 25 MeV/$c^2$ of the nominal $K^0_s$ mass. The opening angle between the flight direction and the momentum vector of the $K^0_s$ candidate is required to be less than 200 mrad, and the transverse flight distance from the primary event vertex must be greater than 2 mm.

Neutral pion candidates are formed from pairs of photons in the EMC with energy above 30 MeV, an invariant mass within 20 MeV/$c^2$ of the nominal $\pi^0$ mass, and a summed energy greater than 200 MeV. A mass-constraint fit is then applied to these $\pi^0$ candidates. The $\pi^0$ from $D^{*+} \rightarrow D^+\pi^0$ decays (“soft” $\pi^0$), however, is required to have an invariant mass within 35 MeV/$c^2$ of the nominal $\pi^0$ mass and momentum in the $\Upsilon(4S)$ frame of $70 < p^* < 450$ MeV/$c$, with no requirement on the summed photon energies.

The decay modes of the $D^0$ and $D^+$ used in this analysis were selected by an optimization of $S^2/(S + B)$ based on Monte Carlo simulations, where $S$ is the expected number of signal events and $B$ is the expected number of background events. The $D^0$ and $D^+$ modes used and their branching fractions are summarized in Table 3. $D^0$ ($D^+$) meson candidates are required to have an invariant mass within 20 MeV/$c^2$ of the nominal $D^0$ ($D^+$) mass.

The $D^{*+}$ mesons are reconstructed in their decays $D^{*+} \rightarrow D^0\pi^+$ and $D^{*+} \rightarrow D^0\pi^0$. We include for this analysis the decay combinations $D^{*+}D^{*-}$ decaying to $(D^0\pi^+, D^0\pi^-)$ or $(D^0\pi^+, D^-\pi^0)$, but not $(D^+\pi^0, D^-\pi^0)$ due to the smaller branching fraction and larger expected backgrounds. The branching fractions for these modes are summarized in Table 3. $D^0$ and $D^+$ candidates are subjected to a mass-constraint fit and then combined with soft pion candidates. A vertex fit is performed that includes the position of the beam spot to improve the angular resolution of the soft pion.

To select $B^0$ candidates with well reconstructed $D^*$ and $D$ mesons, we construct a $\chi^2$ that includes all measured $D^*$ and $D$ masses:

$$\chi^2_{\text{Mass}} = \left( \frac{m_D - m_{PDG}}{\sigma_{m_D}} \right)^2 + \left( \frac{m_{\bar{D}} - m_{\bar{PDG}}}{\sigma_{m_{\bar{D}}}} \right)^2 + \left( \frac{\Delta m_D - \Delta m_{PDG}}{\sigma_{\Delta m_D}} \right)^2 + \left( \frac{\Delta m_{\bar{D}} - \Delta m_{\bar{PDG}}}{\sigma_{\Delta m_{\bar{D}}}} \right)^2$$

(3)
Table 2: $D^0$ and $D^+$ decay modes and branching fractions [9]. The branching fraction for $K_S^0 \to \pi^+\pi^-$ is included for modes containing a $K_S^0$.

| Decay Mode | Branching Fraction (%) |
|------------|-------------------------|
| $D^0 \to K^-\pi^+$ | 3.83 ± 0.09 |
| $D^0 \to K^-\pi^+\pi^0$ | 13.9 ± 0.9 |
| $D^0 \to K^-\pi^+\pi^+\pi^-$ | 7.49 ± 0.31 |
| $D^0 \to K_S^0\pi^+\pi^-$ | 1.85 ± 0.14 |
| Total $D^0$ Branching Fraction | 27.1 |

| Decay Mode | Branching Fraction (%) |
|------------|-------------------------|
| $D^+ \to K^-\pi^+\pi^+$ | 9.0 ± 0.6 |
| $D^+ \to K_S^0\pi^+$ | 0.99 ± 0.09 |
| $D^+ \to K^-K^+\pi^+$ | 0.87 ± 0.07 |
| Total $D^+$ Branching Fraction | 10.9 |

Table 3: $D^*$ and $D^{*0}$ decay modes and branching fractions [9]. $D^{*0}$ is used for the $B^+ \to D^{*+}D^{*0}$ analysis described in Section [3].

| Particle | Decay Mode | Branching Fraction (%) |
|----------|------------|-------------------------|
| $D^{*+}$ | $D^{*+} \to D^0\pi^+$ | 67.7 ± 0.5 |
| | $D^{*+} \to D^+\pi^0$ | 30.7 ± 0.5 |
| Total Visible $D^{*+}$ Branching Fraction | 98.4 |
| $D^{*0}$ | $D^{*0} \to D^0\pi^0$ | 61.9 ± 2.9 |
| | $D^{*0} \to D^0\gamma$ | 38.1 ± 2.9 |
| Total $D^{*0}$ Branching Fraction | 100.0 |

where the subscript $PDG$ refers to the nominal value, and $\Delta m_{D^*}$ is the $D^* - D$ mass difference. For $\sigma_{m_D}$ we use values computed for each $D$ candidate, while for $\sigma_{\Delta m_{D^*}}$ we use fixed values of 0.83 MeV/$c^2$ for $D^{*+} \to D^0\pi^+$ and 1.18 MeV/$c^2$ for $D^{*+} \to D^+\pi^0$. A requirement that $\chi^2_{mass} < 20$ is applied to all $B^0$ candidates. In events with more than one $B^0$ candidate, we choose the candidate with the lowest value of $\chi^2_{mass}$.

A $B$ meson candidate is characterized by two kinematic variables. We use the energy-substituted mass, $m_{ES}$, defined as

$$m_{ES} \equiv \sqrt{E_{Beam}^2 - p_B^*}$$

and the difference of the $B$ candidate’s energy from the beam energy, $\Delta E$,

$$\Delta E \equiv E_B^* - E_{Beam}$$

where $E_B^*$ ($p_B^*$) are the energy (momentum) of the $B$ candidate in the center-of-mass frame and $E_{Beam}^*$ is one-half of the center-of-mass energy. The signal region in the $\Delta E$ vs. $m_{ES}$ plane is defined to be $|\Delta E| < 25$ MeV and $5.273 < m_{ES} < 5.285$ GeV/$c^2$. The width of this region corresponds to approximately ±2.5$\sigma$ in both $\Delta E$ and $m_{ES}$.
These values on $\chi^2_{\text{Mass}}$, $m_{\text{ES}}$, and $\Delta E$ were chosen based on an optimization of $S^2/(S + B)$, where $S$ is the expected number of signal events and $B$ is the expected number of background events. The optimization process was done entirely with samples of signal and generic $B\bar{B}$ and $c\bar{c}$ Monte Carlo where the background distribution is taken from a sideband region, defined as

$$|\Delta E| < 200 \text{ MeV}$$
$$5.20 \text{ GeV}/c^2 < m_{\text{ES}} < 5.26 \text{ GeV}/c^2$$

and

$$50 \text{ MeV} < |\Delta E| < 200 \text{ MeV}$$
$$5.26 < m_{\text{ES}} < 5.29 \text{ GeV}/c^2$$

These values were chosen based on a maximization of $S^2/(S + B)$ with a tendency towards looser cut values to reduce any possible systematic error incurred due to the differences in the reconstructed mass resolutions between data and Monte Carlo.

To determine the number of signal events in the signal region, we must estimate the expected contribution from background. This is done by scaling the number of events seen in the data sideband (defined above) with a scaling factor which gives a measure of the relative areas of the signal region to the sideband region. We parameterize the shape of the background in the $\Delta E$ vs. $m_{\text{ES}}$ plane as the product of an ARGUS function [10] in $m_{\text{ES}}$ and a first-order polynomial in $\Delta E$. Based on this parameterization we estimate that the ratio of the number of background events in the signal region to the number in the sideband region is $(1.72 \pm 0.10) \times 10^{-2}$. The uncertainty is derived from the observed variation of this ratio under alternative assumptions for the background shape in $m_{\text{ES}}$ and $\Delta E$.

Figure 1 shows the events in the $\Delta E$ vs. $m_{\text{ES}}$ plane after all selection criteria have been applied. The small box in the figure indicates the signal region defined above, and the sideband is the entire plane excluding the region bounded by the larger box outside the signal region. There are a total of 38 events located in the signal region, with 363 events in the sideband region. The latter, together with the effective ratio of areas of the signal region to the sideband region, implies an expected number of background events in the signal region of $6.24 \pm 0.33(\text{stat}) \pm 0.36(\text{syst})$. The quoted systematic uncertainty comes from the background shape variation discussed previously. Figure 2 shows a projection of the data on the $m_{\text{ES}}$ axis after requiring $|\Delta E| < 25 \text{ MeV}$.

We use a detailed Monte Carlo simulation of the BABAR detector to determine the efficiency for reconstructing the signal. This, together with the total number of $B\bar{B}$ pairs produced during data collection, allows us to determine a preliminary branching fraction for $B^0 \rightarrow D^{*+}D^{*-}$ to be

$$\mathcal{B}(B^0 \rightarrow D^{*+}D^{*-}) = (8.0 \pm 1.6(\text{stat}) \pm 1.2(\text{syst})) \times 10^{-4}$$

The dominant systematic uncertainty in this measurement comes from our level of understanding of the charged particle tracking efficiency (9.4%). The high charged particle multiplicity in this decay mode makes this measurement particularly sensitive to tracking efficiency. Systematic errors were assigned on a per track basis for $\pi$, $K$ and slow $\pi$, and were added linearly due to large correlations. The imprecisely known partial-wave content of the $B^0 \rightarrow D^{*+}D^{*-}$ final state is another source of systematic biases. Monte Carlo events in each of the two extremes of transversity amplitudes $(A_{//}, \sqrt{2} A_0, A_\perp) = (1, 0, 0)$ and $(0, 1, 0)$ were generated and reconstructed [11]. Although both mixtures correspond to $R_t = 0$, the resulting $p_t$ distributions of the slow pion represent the two extreme cases of possible $p_t$ distributions. The change in the reconstruction efficiency of these
Figure 1: Distribution of $B^0 \rightarrow D^{*+}D^{*-}$ events in the $\Delta E$ vs. $m_{ES}$ plane. The small box indicates the signal region, while the sideband region is everything outside the larger box.

Figure 2: Distribution of $B^0 \rightarrow D^{*+}D^{*-}$ events in $m_{ES}$ plane with a cut of $|\Delta E| < 25$ MeV applied. The curve represents a fit to the distribution of the sum of a Gaussian to model the signal and an ARGUS function [10] to model the background shape.

final angular states is quoted as systematic error (6.6%). Other significant systematic biases arise due to the uncertainties on the $D^{*+}$, $D^0$ and $D^+$ branching fractions (5.6%) and the differences in mass resolutions between Monte Carlo and data (4.1%). Possible contributions from peaking backgrounds was found to be negligible. The total systematic uncertainty from all sources is 14.5%.
Determination of the CP content of $B^0 \to D^{*+}D^{*-}$

The fraction of the CP-odd component, $R_t$, of the decay $B^0 \to D^{*+}D^{*-}$ can be determined from the angular distribution in the transversity basis [3]:

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{tr}} = \frac{3}{4} (1 - R_t) \sin^2 \theta_{tr} + \frac{3}{2} R_t \cos^2 \theta_{tr}$$

(2)

Here $\Gamma$ is the decay rate and $\theta_{tr}$ is the polar angle defined as the angle between the normal to the $D^{*-}$ decay plane and the $\pi^+$ line of flight in the $D^{*+}$ rest frame.

We perform an unbinned maximum likelihood fit to the 38 events in the signal region described in the previous section. The fit takes into account the presence of background, whose properties are derived from the sideband sample, and the angular resolution $\sigma_{\theta_{tr}}$ estimated from the simulated data samples. We define the likelihood function to be

$$L = \prod_{i=1,n} L_i = \prod_{i=1,n} \left[ p \times F(\theta_{tr,i}, \sigma_{\theta,i}, R_{t_{sig}}) + (1 - p) \times F(\theta_{tr,i}, \sigma_{\theta,i}, R_{t_{bkg}}) \right]$$

(3)

where $n$ is the number of selected events and the contribution to the total likelihood from the $i$-th event, $L_i$, is defined in terms of the purity $p$ of the sample and the probability density functions $F(\theta_{tr,i}, \sigma_{\theta,i}, R_t)$ for the signal and background: $R_{t_{sig}}$ and $R_{t_{bkg}}$ are the parameters describing the shapes of the signal and background angular distributions, respectively, and $\theta_{tr,i}$ is the measured transversity angle in event $i$. The probability density functions $F$ are obtained from the convolution of the angular distribution (Eq. 2) with Gaussian resolution functions describing the measurement errors $\sigma_{\theta,i}$. We note that Eq. 2 is the differential decay rate $\Gamma$ integrated over the full ranges of the other two decay angles in the transversity basis; this assumes a flat acceptance and needs to be corrected for in the final determination of $R_t$. An empirical study of the events in the sideband region showed that the background angular distribution can be described as constant in $\cos \theta_{tr}$, as expected. The parameterization in Eq. 3 can describe deviations from this behaviour and was used to estimate the background contribution to the systematic uncertainty on $R_t$.

The fit procedure was tested on several samples of $B^0 \to D^{*+}D^{*-}$ Monte Carlo events generated with different $R_t$ values and different sets of decay amplitudes in order to determine the possible bias induced by angular acceptance effects correlated with the inefficiency in detecting soft pions from $D^*$ decays below a threshold in transverse momentum of about 70 MeV/c. The fitted $R_t$ values were fully consistent with the generated values in the limit of negligible soft pion inefficiency, but could be biased, depending on the decay amplitudes, when the pion detection threshold was taken into account. A correction and a systematic error were estimated to describe these effects (described below).

The value of $R_{t_{bkg}}$ was evaluated by fitting the 363 events in the sideband region and setting $p = 0$ in Eq. 3. The result of this fit was $R_{t_{bkg}} = 0.29 \pm 0.04$, compatible with the value expected for a flat distribution ($R_t = 1/3$).

To determine $R_{t_{sig}}$, we fit the 38 events in the signal region with $R_{t_{bkg}}$ fixed to 0.29 and $p$ fixed at 83.6%. The result of the fit to the signal region, without correction for angular acceptance bias, is $R_{t_{sig}} = 0.25 \pm 0.18$(stat), and is shown in Figure 3. The fit was repeated with both $R_{t_{sig}}$ and $R_{t_{bkg}}$ floating, giving the same central values with a rather small correlation (~0.04) between the parameters.
Figure 3: The $\cos \theta_{tr}$ distribution from the unbinned ML fit, superimposed on the histogram of the $B^0 \rightarrow D^{*+}D^{*-}$ candidates in the signal region. The dotted and dashed lines represent the fitted CP components for the signal and background contributions. The lower two dotted curves represent the two background fitted components, proportional to $\sin^2 \theta_{tr}$ and $\cos^2 \theta_{tr}$ respectively; their sum (dashed curve) is almost constant at about 0.3 events/bin. Similarly, the two upper dashed curves represent the CP components of the signal. The solid line represents the $\cos \theta_{tr}$ distribution from the unbinned ML fit for the selected events.

The dominant systematic uncertainty on the measured value of $R_t$ comes from the acceptance bias due to the transverse momentum threshold in the detection of soft pions. This bias ranges between $-0.048$ and $+0.004$, and depends on the yet unknown decay amplitudes. The central value of this interval was taken as a correction to the fitted $R_t^{\text{sig}}$, while its half width was assumed as a contribution to the systematic error. Other contributions come from the imperfect knowledge of the finite resolution on the measured value of $\theta_{tr}$ ($0.006$), of the angular distribution of the background ($0.008$) and of the purity of the signal sample ($0.0003$). All uncertainties were evaluated with Monte Carlo simulations. The total systematic uncertainty on $R_t$ was determined to be $0.031$, giving the final corrected result:

$$R_t = 0.22 \pm 0.18(\text{stat}) \pm 0.03(\text{syst})$$

The likelihood function was also used to estimate approximate confidence intervals, taking into account the allowed physical region. Fig. 4 shows the dependence of $L_{\text{data}}(R_t) = -2 \ln(\mathcal{L}(R_t)/\mathcal{L}(\bar{R}_t))$ on $R_t$, where $\bar{R}_t$ is the value of $R_t$ that maximizes $\mathcal{L}(R_t)$. The lines corresponding to the 68%, 95%, 99% confidence level limits on $R_t$ are also plotted. We can exclude values of $R_t$ greater than 0.63 at the 95% confidence level.
Figure 4: Likelihood ratio $L_{\text{data}}(R_t) = -2\ln(\mathcal{L}(R_t)/\mathcal{L}(\bar{R}_t))$ for the data, where $\bar{R}_t$ is the value of $R_t$ that maximizes $\mathcal{L}(R_t)$, and 68%, 95%, 99% confidence level limits on $R_t$. The systematic error on $R_t$ is indicated by the dotted and dashed lines.

5 Observation of the decays $B^0 \to D^{*+}D^-$ and $B^+ \to D^{*+}D^{*0}$

The decays $B^0 \to D^{*+}D^-$ and $B^+ \to D^{*+}D^{*0}$ are studied following a method largely similar to that described in Sec. 3. Here, only those aspects of the analyses that differ significantly from that of the $B^0 \to D^{*+}D^{*-}$ analysis are discussed in some detail.

For $B^0 \to D^{*+}D^-$, $B^0$ mesons are exclusively reconstructed by combining a $D^{*\pm}$ and a $D^{\mp}$ candidate that are reconstructed in a number of $D^{*\pm}$ and $D^{\mp}$ decay modes. For $B^+ \to D^{*+}D^{*0}$ the exclusive reconstruction combines a $D^{*\pm}$ and a $D^{*0}$. The kaon flavor of the $D^{*0}$ is checked to make sure that a $D^{*+}$ is paired only with a $D^{*0}$ and a $D^{*-}$ is only paired with a $D^{*0}$. The selection of $D^{\pm}$ and $D^{*\pm}$ candidates, and the $K^0_S$ and $\pi^0$ candidates that are used to compose them, is identical to that described for the $B^0 \to D^{*+}D^{*-}$ analysis.

The decay modes of the $D$ and $D^*$ used in these analyses are selected by an optimization of $S^2/(S + B)$ based on Monte Carlo simulations. $D^{\pm}$ mesons are reconstructed in their decays $D^{*\pm} \to D^0\pi^\pm$ and $D^{*+} \to D^+\pi^0$, and $D^{*0}$ mesons are reconstructed in their decays $D^{*0} \to D^0\pi^0$ and $D^{*0} \to D^0\gamma$. Modes used and their branching fractions are summarized in Tables 2 and 3. As in the $B^0 \to D^{*+}D^{*-}$ analysis, we construct $\chi^2_{\text{Mass}}$ variables that include all measured $D^{*\pm}$, $D^{*0}$, and $D$ masses. For $B^+ \to D^{*+}D^{*0}$, $\chi^2_{\text{Mass}}$ contains 4 terms:
\[ \chi^2_{\text{Mass}} = \left( \frac{m_D - m_{PDG}}{\sigma_D} \right)^2 + \left( \frac{m_{D^*} - m_{PDG}}{\sigma_D} \right)^2 + \frac{\left( \Delta m_{D^*} - \Delta m_{PDG} \right)}{\sigma_{\Delta m_{D^*}}} \]

For \( B^0 \rightarrow D^{*+}D^- \), \( \chi^2_{\text{Mass}} \) contains 3 terms:

\[ \chi^2_{\text{Mass}} = \left( \frac{m_D - m_{PDG}}{\sigma_D} \right)^2 + \left( \frac{m_{D^*} - m_{PDG}}{\sigma_{D^*}} \right)^2 + \frac{\left( \Delta m_{D^*} - \Delta m_{PDG} \right)}{\sigma_{\Delta m_{D^*}}} \]

The major difference between these analyses and the \( B^0 \rightarrow D^{*+}D^{*0} \) analysis is that the \( \chi^2_{\text{Mass}} \) cut values for these analyses are set individually for each submode instead of having a global \( \chi^2_{\text{Mass}} \) value for all submodes, to better take into account the fact that the amount of background is quite different for each of the different submodes in these analyses. The procedure used to optimize the \( \chi^2_{\text{Mass}} \) value chooses the individual values of \( \chi^2_{\text{Mass}} \) that together maximize the global \( S^2/(S+B) \). Submodes which have an optimal value of less than 2 times the number of degrees of freedom of the \( \chi^2_{\text{Mass}} \) (8 for \( B^+ \rightarrow D^{*+}D^{*0} \), 6 for \( B^0 \rightarrow D^{*+}D^- \)) are rejected on the grounds that the resulting sensitivity is poor, and that the tightness of the \( \chi^2_{\text{Mass}} \) value makes such modes more susceptible to systematic errors in measured yield.

These values were tuned with samples of signal and generic \( B\bar{B} \) and \( c\bar{c} \) Monte Carlo where the background distribution is taken from a sideband region. For \( B^+ \rightarrow D^{*+}D^{*0} \), the sideband region is the same as that for \( B^0 \rightarrow D^{*+}D^- \). For \( B^0 \rightarrow D^{*+}D^- \), the region where decays (such as \( B^0 \rightarrow D^{*+}D^- \)) can feed down into the \( \Delta E - m_{ES} \) plane must be eliminated from the sideband. As \( B^0 \rightarrow D^{*+}D^{*0} \) contains a reconstructed \( D^{*0} \) and \( D \), it is only separated from \( B^0 \rightarrow D^{*+}D^- \) events due to the missing energy of the slow pion from the second \( D^{*\pm} \). This missing energy manifests itself as a negative shift in \( \Delta E \). These events accumulate in the area below the \( B^0 \rightarrow D^{*+}D^- \) signal region, and in order to remove them, the region defined by:

\[ \Delta E < -50 \text{ MeV} \]

\[ m_{ES} > 5.26 \text{ GeV}/c^2 \]

is removed. The \( m_{ES} \) and \( \Delta E \) distributions for events reconstructed in the channels \( B^0 \rightarrow D^{*+}D^- \) and \( B^+ \rightarrow D^{*+}D^{*0} \) are shown in Fig. 5 and in Fig. 6.

For the \( B^0 \rightarrow D^{*+}D^- \) channel we reconstruct a total of 31 events, of which 10.5 ± 1.7(stat) are background. The probability that the visible signal is a statistical fluctuation of the background is \( 9.7 \times 10^{-7} \) (> 4.3\( \sigma \)). As pointed out in the introduction, this channel is a \( CP \) conjugate state that can be used for \( \sin2\beta \) measurements. For \( B^+ \rightarrow D^{*+}D^{*0} \) we reconstruct a total of 39 events, of which 20.3 ± 0.5(stat) are background. The probability that the visible signal is a statistical fluctuation of the background is \( 2.9 \times 10^{-6} \) (> 4.1\( \sigma \)). This channel is useful for calibrations and tests of the \( CP \) fitting procedures.

6 Summary

Using data collected by the \( BABAR \) experiment during 1999-2000, we have observed a signal of \( 31.8 \pm 6.2 \) (stat) ± 0.4(syst) events in the decay \( B^0 \rightarrow D^{*+}D^{*0} \). Our measurement of the branching
**Figure 5:** Top Left: $m_{\text{ES}}$ projection of the $B^0 \to D^{*+}D^-$ event population, in the $\Delta E$ signal band ($-0.025 < \Delta E < 0.025 \text{ GeV}$). The crosses are the data. The dashed line represents the extrapolation, to the $\Delta E$ signal band, of a two-dimensional background fit in the $\Delta E$-$m_{\text{ES}}$ sidebands. The solid line is the sum of this background extrapolation and of a fitted, Gaussian-shaped signal centered on the $B$ mass. Top Right: $\Delta E$ projection of the $B^0 \to D^{*+}D^-$ event population, in the $m_{\text{ES}}$ signal band ($5.273 < m_{\text{ES}} < 5.285 \text{ GeV/c}^2$). The crosses are the data. The dashed line represents the extrapolation, to the $m_{\text{ES}}$ signal band, of the above-mentioned background fit. The solid line is the sum of this background extrapolation, and of a gaussian-shaped signal centered on $\Delta E = 0$. In the case of both the upper plots, the points in the feed-down region ($\Delta E < -0.05 \text{ GeV}$) are excluded from the fits. Bottom: Two-dimensional distribution of the $B^0 \to D^{*+}D^-$ events in the $\Delta E$ vs. $m_{\text{ES}}$ plane. The small ellipse indicates the signal region, while the sideband region is everything that is outside the box that surrounds the signal region and also outside the (feed-down) box below the signal region.
Figure 6: Top Left: $m_{ES}$ projection of the $B^+ \rightarrow D^{*+}D^{*0}$ event population, in the $\Delta E$ signal band ($-0.025 < \Delta E < 0.025 \text{GeV}$). The crosses are the data. The dashed line represents the extrapolation, to the $\Delta E$ signal band, of a two-dimensional background fit in the $\Delta E - m_{ES}$ sidebands. The solid line is the sum of this background extrapolation and of a fitted, Gaussian-shaped signal centered on the $B$ mass. Top Right: $\Delta E$ projection of the $B^+ \rightarrow D^{*+}D^{*0}$ event population, in the $m_{ES}$ signal band ($5.273 < m_{ES} < 5.285 \text{GeV}/c^2$). The crosses are the data. The dashed line represents the extrapolation, to the $m_{ES}$ signal band, of the above-mentioned background fit. The solid line is the sum of this background extrapolation, and of a Gaussian-shaped signal centered on $\Delta E = 0$. Bottom: Two-dimensional distribution of the $B^+ \rightarrow D^{*+}D^{*0}$ events in the $\Delta E$ vs. $m_{ES}$ plane. The small ellipse indicates the signal region, while the sideband region is everything that is outside the box that surrounds the signal region.
ratio is
\[ \mathcal{B}(B^0 \to D^{*+}D^{*-}) = (8.0 \pm 1.6(stat) \pm 1.2(syst)) \times 10^{-4} \]

From the transversity angular distribution of these events, the measured fraction of the component with odd \( CP \) parity is
\[ R_t = 0.22 \pm 0.18(stat) \pm 0.03(syst) \]

Finally, signals are also observed in the decay modes \( B^0 \to D^{*+}D^- \) and \( B^+ \to D^{*+}D^0 \).

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[1] Charge-conjugate states are implied throughout this paper and the symbol \( D^{(*)} \) refers to either \( D \) or \( D^* \).

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