New features for delamination depth evaluation in carbon fiber reinforced plastic materials using eddy current pulse-compression thermography

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Abstract: The growing application of composite materials in aerospace leads to the urgent need of non-destructive testing and evaluation (NDT&E) techniques capable of detecting defects such as impact damage and delamination possibly existing in those materials. Eddy current pulsed thermography is an emerging non-destructive testing (NDT) technique capable of detecting such defects. However, the characterization of delamination within composite materials is difficult to be achieved by a single pulse excitation especially in carbon fiber reinforced plastic materials as the extraction of thermal diffusion in such multi-layered structures is challenging. To cope with this problem, this paper proposes the eddy current pulse-compression thermography (ECPuCT) combining the Barker code modulated eddy current excitation and pulse-compression technique to enhance the capability of characterizing delamination on carbon fiber reinforced plastic materials. Additionally, a thermal pattern enhanced method based on kernel principal component analysis technique is used to locate the delaminated areas. Two features, including a newly proposed crossing point of impulse responses related to defective and non-defective areas and skewness of impulse responses are investigated for delamination depth evaluation. Results show that delamination can be detected within depths ranging from 0.46 mm to 2.30 mm and both the proposed features have a monotonic relationship with delamination depths.

Keywords: Pulse-Compression; Eddy Current Pulsed Thermography; Feature extraction; Carbon Fiber Reinforced Plastic; Delamination depth; Barker code

1. Introduction

The use of Carbon Fiber Reinforced Plastic (CFRP) materials has become increasingly popular among conventional engineered materials due to their extraordinary mechanical and thermal properties, such as high strength-to-weight ratio, corrosion resistance, improved fatigue performance and low coefficient of thermal expansion [1]. Delamination is one of the most common defects for composite materials, which might arise either during the manufacturing process or during their in-service life, e.g. during the standard lifetime of aircraft components. A typical delamination initiates and grows between different plies of the composite, which may result in lowered in-plane strength and stiffness, eventually leading to catastrophic failure of the whole structure [2].

To detect delamination and ensure the safe operation of composite components, NDT techniques are used during both manufacturing and operation of the composite components. As an example, Ultrasonic Testing (UT) can locate the substantial flaws in CFRP via ultrasonic waves with frequencies usually ranging from hundreds of kHz to several tens of MHz [3].

However, ultrasonic wave can be attenuated either by the geometry and anisotropy or via viscoelastic absorption loss in resin and multiple scattering loss caused by fibers. As a
consequence, delamination echoes are possibly buried in noise, thus computationally-expensive post-processing algorithms are often required to implement fruitfully the feature extraction [4]. X-Ray Computed Tomography (XCT) can provide both qualitative and quantitative information for a comprehensive understanding of delamination initiation and evolution, but the cost in terms of experimental setup (software and hardware) and the complexity of measurements makes such test quite challenging to be performed routinely [4].

A promising NDT technique to detect delamination in CFRP is the Active Thermography (AT) [5, 6]. Being a non-contact method with the capability of inspecting a large area of the Sample Under Test (SUT), AT has been extensively used for inspecting CFRP in a number of different application scenarios [7], as well as for material characterization [8, 9], cultural heritage diagnostic [10], on-line monitoring of goods in different production plants [11, 12]. In AT, the desired thermal contrast is achieved by applying an external heating stimulus over the SUT [13] by means of various different physical sources. Light sources are the most common, see for instance [14-19], the SUT’s illuminated surface heats up and then the heat diffuses toward the inner side of the sample to restore thermal equilibrium [20]. Alternatively, other methods of excitation have been proposed and successfully applied such as Ultrasound Vibro-Thermography [21], Eddy-Current Pulsed Thermography (ECPT) [22] and Microwave Thermography [23]. Among these, one of the extensively applied AT technique is ECPT. ECPT uses a coil driven by alternating current to generate EC inside the SUT that increases temperature due to the Joule effect. Since CFRP exhibits low electrical conductivity, in most of the ECPT cases the stimulation can be considered volumetric since the typical eddy-current skin depths is greater than or comparable with the sample thickness [24]. For this reason, ECPT is also poorly influenced by the surface conditions of the SUT [18]. Despite the progresses made on ECPT, both for evaluating the so-called barely invisible impact damage [24-26] and visualizing delamination [27-29], the quantitative evaluation of the delamination depth is still challenging. In fact, the complex structure of CFRP, i.e. layered structure, anisotropic conductivity and different fiber direction, results in non-uniform thermal distribution, thus hampering the faithful quantitative evaluation of the delamination depth from the thermal response.

To gain insight about the here-proposed approach, it is worth briefly resume here the possible ways in which AT can be performed. Despite the employed heating source, the classification of the AT schemes is strictly related to the time-frequency characteristic of the heating modulation signal. In Pulsed Thermography (PT), a short time duration heating stimulus - usually of few milliseconds- excites the SUT within an extended bandwidth. The duration of the pulse is significantly shorter than typical heat diffusion phenomena in the SUT, so that the excitation pulse well-approximates the Dirac’s delta δ(τ). Features extraction can be performed by analysing both the heating and the cooling trends of the recorded impulse response h(τ) pixelwise. Note that the maximum achievable value of the SNR in PT is set by the employed excitation source power. Improved SNR values might be obtained by concentrating the heating stimulus energy within a narrow frequency range as in the Lock-in Thermography (LT) scheme, wherein the heating stimulus is modulated with a sinusoid at given frequency. The main drawback of LT is the less amount of possible information obtainable with respect to PT [30], which is a direct consequence of the narrower bandwidth of the heating stimulus. Furthermore, if the delamination depths are aimed at being characterized by LT, an improper choice of the modulation frequency might lead to thermal diffusion length values that do not match properly the possible defects depths [24].

In the last decades, efforts have been made to merge the effectiveness of PT and the SNR values achievable via LT, leading for examples to Pulsed Phase Thermography and Multi-Frequency Lock-in Thermography [31, 32]. An alternative approach exploits the positive features of Pulse-compression (PuC) technique and coded excitations. The use of coded excitation signals and PuC in thermal phenomena has been pioneered by research groups led by Mandelis [33] and Mulavesesala [34]. Subsequently, various Pulse-Compression Thermography (PuCT) procedures have been proposed [35, 36]. The PuC algorithm outputs a good estimate of impulse response that is close in both characteristics and quality to that obtainable from PT. In PuCT, the heat source emission is commonly modulated either by a frequency-modulated
“Chirp” signal [37], or by a phase-modulated signal [34], e.g. Barker code. These coded excitations have a characteristic trait: their bandwidth $B$ and their time duration $T$ are uncorrelated. This means that the frequency content of the coded signal can be tailored to suit the investigation of a given sample, while $T$ can be increased almost arbitrarily to achieve the desired SNR [38, 39]. In addition, both time and frequency domain analyses can be performed for characterizing the investigated material when coded excitations are used. In particular, the time analysis can be retrieved after the application of the PuC algorithm, whilst a frequency analysis can be directly implemented on the raw acquired data. Although PuCT is now a quite established technique that shows promises for maximizing the SNR even when low power heat sources are employed, very few attempts are reported in literature to extend this approach to ECPT [40, 41].

Based on the above-mentioned PuC features, the aims of this work are (i) to increase the detectability of delamination and (ii) to evaluate them quantitatively on an artificially-delaminated CFRP sample by using coded waveforms and PuC technique in ECPT. Hereinafter, such a combination will be referred as Eddy Current Pulse-Compression Thermography (ECPuCT).

Fig. 1 shows the block diagram of the overall process to extract features for the delamination depths characterization using ECPuCT. Each block of this diagram, numbered from 1 to 4, shows the steps followed in this study to extract the final feature. ECPuCT method is firstly applied on the CFRP benchmark sample containing manmade delamination defects at different depths and the raw data in the form of thermograms are acquired, as for block 1. Then a denoising algorithm is applied on each individual pixel’s signal to remove noise and a non-linear fitting function is also exploited to remove the step-heating contribution from the denoised data as explained in [19], see Fig. 1 block 2. Then, as showed in block 3, the calculation of the impulse response $h(t)$ is performed by convolving the de-trended signal with a matched filter. After obtaining the impulse response $h(t)$ of each individual pixel, the feature extraction process is carried out, as depicted in block 4. Kernel Principal Component Analysis (K-PCA) technique is used on the retrieved $h(t)$’s to obtain principal components and to enhance delaminated areas. Based on the enhanced delaminated area, the impulse responses including delaminated and non-delaminated areas are selected manually. Different features including the proposed crossing point of $h(t)$’s and skewness of defective area impulse response are validated and compared for delamination depth evaluation.

This paper is organized as follows: Section 2 presents the theoretical background of EC stimulated heating, the basic theory of PuC, the proposed methodology of impulse response based thermal enhanced pattern technique and the feature extraction process. Section 3 provides details about the Barker code excitation, the ECPuCT experimental setup and the benchmark delaminated CFRP sample. Section 4 shows how to perform PuC correctly and highlights the

**Fig. 1** Block diagram of the processing steps of proposed feature extraction and validation
analysis of various extracted thermal pattern by the proposed technique. The validation of the proposed feature is also conducted through experiment. Conclusion will be made in Section 5.

2. Theoretical background of eddy current pulse compression thermography and proposed feature extraction

2.1 Theory of eddy current stimulated volumetric heating in CFRP

The theory of ECPT on ferromagnetic material has been addressed in previous researches [42-44]. The principle of ECPT for CFRP is different from that of ferromagnetic materials, concerning both the heating mode and the thermal wave diffusion pattern. According to Eq.(1), the penetration depth $\delta$ of an electromagnetic wave into a conductive material has a monotonic decreasing relationship with increasing current frequency:

$$\delta = \frac{1}{\sqrt{\pi \mu \sigma f_{\text{carrier}}}}$$

where $f_{\text{carrier}}$ is the frequency of the excitation current [Hz], $\sigma$ is electrical conductivity [S·m$^{-1}$], and $\mu$ is magnetic permeability [H·m$^{-1}$]. In general, for CFRP the bulk conductivity $\sigma$ value is in the order of 15000 S·m$^{-1}$ and it is non-magnetic [45]. Considering an $f_{\text{carrier}} = 300$ kHz, the corresponding penetration depth is 7.5 mm while for the same value of $f_{\text{carrier}}$, the penetration depth in steel ($\sigma = 9.93 \times 10^6$ S/m, $\mu = 3.77 \times 10^{-4}$ H/m) is equal to 29.08 $\mu$m, which is significantly smaller than one obtained for CFRP. Thus, since the thickness of the CFRP sample is often lower than corresponding value of $\delta$, the heating mode is volumetric.

Due to skin effect, the eddy current density has an exponential decay in through-thickness direction. Therefore, the heat generated through Joule effect at different layer of composites decays exponentially through the perpendicular direction.

The thermal response in CFRP can be recognized as a sum of thermal waves. Each of them has a different frequency $f$, thermal diffusion length $\mu$, and diffusion velocity $v$. According to thermal wave theory, $\mu$ can be expressed as:

$$\mu = \sqrt{\frac{k}{\pi f \rho c}} = \frac{\alpha}{\sqrt{\pi f \alpha}} \quad \text{(2)}$$

where $k$ is thermal conductivity, $\rho$ is density [$g \cdot m^{-3}$], $C$ is heat capacity [$J \cdot g^{-1} \cdot K^{-1}$], and $\alpha$ is thermal diffusivity [$W \cdot m^{-1} \cdot K^{-1}$]. The diffusion velocity $v$ can be obtained as:

$$v = \sqrt{4\pi f \alpha} \quad \text{(3)}$$

Equations (2) and (3) indicate that thermal waves having higher frequencies diffuse faster but shallower, while low frequency thermal waves diffuse slower but deeper into the sample. If there is a defect at some depth, the parameters (like amplitude and phase) of the thermal wave will change, thus allowing the flaws to be detected by an InfraRed (IR) camera.

In the case of volumetric heating, the ECPT characterization can be either in transmission or reflection mode. The transmission and reflection arrangements are depicted in Fig.2 (a).

![Fig. 2](image-url) Eddy current pulsed thermography measurement modes, (a) Configuration of transmission mode and reflection mode; (b) Comparison of Surface heating and Volumetric heating
the thermal diffusion length \( \mu \) is greater than depth \( d \) at which the delamination/defect is possibly buried, response from the defect can be observed through the acquired surface temperature field. The unique advantage of volumetric heating compared to the surface heating scenarios (e.g. as in the case of light-stimulated thermography) comes from the direct interaction between the buried defect and the induced eddy current field, see Fig.2 (b). In surface heating mode, the generated thermal wave must be reflected by the defect, taking twice the time with respect to the volumetric heating mode before being recorded by the IR camera. Overall, the heating pattern of the EC excitation in transmission arrangement can be considered as follows: firstly, the whole specimen is heated-up by the induced eddy current and Joule’s effect [26]. Then, the defected area is heated more than the sound areas at the same depth. The information needed for characterizing the defects comes from the thermal wave travelling from the defected area at a depth \( d \), as shown in Fig.2 (a), where \( t_r \) and \( t_d \) represent the travelling time of the thermal response from defect to the surface in transmission and reflection modes respectively.

2.2 Pulse compression basic theory

This section will give detailed explanation of PuC techniques. PuC is a wide-spread measurement technique used to experimentally estimate the impulse response of a Linear Time Invariant (LTI) system in a noisy environment or in presence of very low SNR values [46]. In standard PT, flash lamps are commonly employed to excite the sample -assumed as an LTI system- within a time significantly shorter than the typical cooling time of the sample itself. Therefore, the so-provided heating stimulus can be modelled as a Dirac’s Delta function \( \delta(t) \), and the corresponding output \( y(t) \), i.e. the pixel temperature/emissivity amplitude recorded with the elapsing time, is a good approximation of the impulse response \( h(t) \) [19]. Features of interest are obtained by analyzing the \( h(t) \) within a chosen range of interest \( T_h \) as showed in Fig.3 (b). As it is shown in Fig.3 (a), in PT the excitation is considered instantaneous and the sample impulse thermal response is measured for a time of interest \( T_h \), which is the impulse response time duration. In PuCT, the sample is excited with a coded excitation of duration \( T \) and thermograms are collected for an overall time duration of \( T + T_h \). An estimated impulse response of duration \( T_h \) is retrieved after performing the PuC algorithm (i.e. the duration of the equivalent PT analysis) [19,36].

PuC requires further processing to achieve an estimate \( \hat{h}(t) \) of the impulse response \( h(t) \), the quality of the estimation depending strictly on both the correct implementation of the PuC algorithm and on the correct design of the coded signal [37]. The working principle of the PuC technique is sketched in Fig.3 (b). Given a coded excitation \( s(t) \) of duration \( T \) and bandwidth \( B \), and another signal \( \Psi(t) \), the so-called matched filter, such that their convolution “∗” approximates the Dirac’s Delta function \( \delta(t) \) as:

\[
s(t) ∗ \Psi(t) = \delta(t) \approx \delta(t)
\]  

then an estimate \( \hat{h}(t) \) of the \( h(t) \) is obtained by convolving the recorded output signal \( y(t) \) with the matched filter \( \Psi(t) \). The process is mathematically showed below for a single pixel of the acquired thermograms, in the presence of an Additive-White-Gaussian-Noise \( e(t) \), which is uncorrelated with \( \Psi(t) \). By convolving the output signal \( y(t) \) with the matched filter \( \Psi(t) \), the impulse response can be obtained as:

\[
\hat{h}(t) = y(t) ∗ \Psi(t) = h(t) ∗ s(t) ∗ \Psi(t) + e(t) ∗ \Psi(t) = h(t) ∗ \delta(t) + e(t) ≈ h(t) + \bar{e}(t)
\]  

The main advantages of PuC over pulsed excitation is that an estimate of the impulse response can be achieved at end of the procedure, while delivering energy to the system over an extended time. In this way, it is possible to provide more energy, and hence to increase the SNR and detectability of eddy current thermography system. The SNR gain is proportional to the \( T × B \) product, i.e. it can be enhanced almost arbitrarily by increasing either the time duration or the bandwidth of the coded waveform. It should be also noted that the limited \( T × B \) product of practically-employed coded signals results in an \( \hat{h}(t) \) always affected by sidelobes. This can be improved by a proper choice of the matched filter signal \( \Psi(t) \) [47]. In this paper, \( s(t) \) is a Barker Code (BC) of order equal to 13 and the matched filter \( \Psi(t) \) has been chosen.
simply to be the time-reversed sequence of the input coded signal \( s(-t) \) [48]. Details about the BC signal and how to implement it in ECPuCT will be shown in the next section. A thorough analysis of PuC lies beyond the scope of this work, for a detailed discussion of PuC can be found in [39].

2.3 Impulse response feature extraction process

This section will give detailed explanation of process in the block 4 of Fig.1. After calculating estimated impulse response \( \hat{h}(t) \), the Kernel Principal Components Analysis (K-PCA) method is applied to locate the delaminated area and select abnormal pixels for feature extraction. The crossing point between defective area and non-defective area are selected for depth evaluation, of which the process is presented in Fig 4.

Two different features including crossing point and skewness are extracted based on the selected impulse response. The crossing point is defined as the first cross point of the impulse response curves onto defective area and non-defective area. The specific calculation of skewness to characterize the impulse responses’ shape is presented in [49]. To calculate the features, the first 200 frames of \( T_h \) was used, which is shown in fig. 4 and fig.10. The reason for using this period is that previous studies [19, 36] has shown that the range of interest of the collected impulse response is limited to less than 10 seconds for reflection mode PuCT analysis. Therefore, 200 frames have been here selected for the feature extraction in transmission mode, which corresponds to 4 seconds of diffusion time when an acquisition frame rate of 50 FPS is employed. Moreover, the so-called “sidelobes” affecting the estimated impulse response would affect otherwise the feature’s performance, e.g. reducing the sensitivity of proposed feature for depth evaluation.

The novel thermal pattern enhancement method is based on K-PCA method. Compared with the traditional imaging PCA, this method considers the impulse response of each pixel rather than each image in the thermal video as independent variables. Each extracted PC is a linear combination of the original impulse response and they form the basis of the respective vector space, arranged in order of decreasing variance. Thus, the first several PCs carry the most information regarding the original data [48].

**Fig. 3** Estimation of impulse response: (a) single pulse excitation, (b) Process of impulse response calculation
To gain insight on how K-PCA is applied here for enhancing ECPuCT data, the implementation of the enhancement method is schematically depicted in Fig.4 (b) and mathematically introduced here below. Considering the calculated impulse response $\hat{h}$’s retrieved pixelwise by exploiting the procedure described in Eq.(5) being reshaped as:

$$[\hat{h}_1, \hat{h}_2, ..., \hat{h}_M],$$

where $M$ is equal to $N_x \times N_y$ denotes the total number of x and y pixel of the acquired IR thermograms. Thus, the reshaped data can be recognized as a matrix having dimension of $Q \times M$, where $Q$ denotes the number of frames recorded by the IR camera, i.e. $T_h \times \text{FPS}$, where FPS stands for the acquired Frames Per Second. By using the kernel method, the impulse response is projected to kernel space $\phi$, thus obtaining the kernel matrix $K(i,j)$ as:

$$K(i,j) = \frac{1}{M} \sum_{i=1}^{M} \left( \phi(\hat{h}_i) - \frac{1}{M} \sum_{j=1}^{M} \phi(\hat{h}_j) \right) \left( \phi(\hat{h}_i) - \frac{1}{M} \sum_{j=1}^{M} \phi(\hat{h}_j) \right)^T,$$

where $\phi$ is Gaussian kernel function, defined as Eq.(8):

$$\phi(\hat{h}_i, \hat{h}_j) = \exp\left(\frac{||\hat{h}_i - \hat{h}_j||_2^2}{2\sigma^2}\right).$$

The kernel matrix $K(i,j)$ of Eq.(7), can be simply named as $K$. The eigenvector $\alpha$ of $K$ can be obtained as:

$$\lambda_i \alpha_i = K \alpha_i$$

Based on the obtained eigenvectors $\alpha_i$, the enhanced thermal pattern can be projected as:

$$H_{\text{enhanced}} = [\alpha_1, ..., \alpha_T]H_{\text{original}}^T,$$

where $H_{\text{enhanced}}$ contains different extracted thermal patterns.

After obtaining different thermal patterns projected by different PCs, in this paper PC2 and PC3 are exploited for differential computation as shown in Fig.12 to enhance the delaminated area, which will be discussed in section 4.2.

3. Experimental setup of eddy current pulse compression thermography
3.1 Barker code implementation in eddy current pulse compression thermography

This section describes the process of the block 1 in Fig.1, in which the coded signal employed for modulating the induction heating system on/off state was a bipolar BC with a bit length of 13. However, the BC code is not employed in its original bit version in PuCT application. In fact, each “1” and “-1” of the original BC code is padded with a series of “1” or “-1” respectively to allow the heat source spreading enough energy toward the SUT. In addition, changing the single bit duration varies the frequency spectrum of the resulting BC modulated heating stimulus. This means that a proper design of the BC code leads to the onset of thermal waves having a desired yet needed thermal diffusion lengths $\mu$, allowing defects buried at different depths to be detected. The thermal diffusion lengths $\mu$ can be calculated by Eq.(5), by considering both the diffusivity $\alpha$, and the frequency $f$ value of the modulated thermal frequency spectrum at which the maximum heat emission occurs, i.e. 0.5 Hz in this case. Fig.5(a) shows the employed BC signal in which, each single bit lasts one second at the chosen FPS (50 frames per second), whilst its thermal frequency spectrum is depicted in Fig.5 (b).

In the implementation of ECPuCT, the chosen BC modulates the induction heating unit, i.e. the on/off time instant at which a current $I$ of given amplitude $Amp$ and frequency $f_{carrier}$ flows within the coil. Fig.6 shows a sketch of the modulated EC signal by BC in ECPuCT.

![Fig. 5 Barker Code signal as implemented](image)

![Fig. 6 A sketch of the modulated EC signal by Barker Code in ECPuCT used in the study](image)

3.2 Eddy current pulse compression thermography setup

The ECPuCT system diagram is illustrated in Fig.7 (a). Signal generator is used to send both the BC modulating signal to the induction heating coil and a reference clock trigger to the IR camera to acquire thermograms at 50 FPS. A Cheltenham EasyHeat 224 Induction heating unit is used for coil excitation with a maximum excitation power and current values of 2.4 kW and 400 A respectively with tunable $f_{carrier}$ from 150 to 400 kHz. For the reported experimental results, values of excitation current $I$ equal to 40 A and $f_{carrier}$ of 240 kHz were selected to avoid eventual damage on the CFRP sample due to the long excitation time using BC signal.
Fig. 7 (b) shows a picture of the employed rectangular coil made of a high-conductivity hollow copper tube. Water cooling was implemented to the coil and the lift-off maintained at 3 mm from the SUT surface to ensure the volumetric heating of the sample. Only one side of the coil is selected as linear coil to introduce parallel eddy currents in the direction of maximum conductivity in the sample. IR camera was the FLIR SC655, equipped with an un-cooled microbolometer detector array with the resolution of 640×480 pixels, the spectral range of 7.5 - 14.0 µm and NETD < 30 mK. The IR camera records the surface temperature distribution of the 13 s BC as well as additional 30 seconds of cooling period [19]. Finally, captured thermal videos were transmitted to a PC for visualization and postprocessing, including signal pre-process, PuC, thermal pattern enhancement and depth feature extraction.

3.3 Sample under test

The CFRP laminate sample was realized at University of Perugia [19] and contains twelve plies of carbon fiber fabric with an areal density of 0.2 g/m². Its lateral dimensions are 240 mm×200 mm for an overall thickness of ~2.80 mm. The fibers orientations are 0° and 90° and the matrix is an Epoxy Resin RIM 935. The laminate was made by vacuum assisted resin infusion and it was cured at room temperature and postured at 110 °C for two hours to obtain a fully cured system. The artificial delamination defects were realized by inserting thin square pieces of Teflon tape having lateral dimensions of 20 mm×20 mm and thickness equal to 75 µm between the plies as shown in Fig.8 (a). Nine artificial defects were inserted at increasing depths: defect #1, the shallowest, was placed under the 2nd ply at a depth $d$~0.46 mm and defect #9t, the deepest, was under the 10th ply at a depth of $d$~2.3 mm in the sample as shown in Fig. 8 (b).
4. Results and analysis

4.1 Process of obtaining estimated impulse response

As discussed in section 3.1, the BC excitation is applied to generate raw data. As block 2 of Fig.1 shows, the raw acquired data must be pre-processed before successfully applying the PuC algorithm to obtain estimated impulse response: the raw acquired data contains (i) noise generated during the signal acquisition process and (ii) an additional step-heating contribution due to the monopolar heating source that must be removed.

Regarding point (i), although the PuC algorithm acts as a low-pass filter as it is based on the convolution with a bandlimited matched filter signal $\Psi(t)$ (see Eq. (5)), it is crucial to minimize the noise to ensure a successful feature extraction of delamination depth. To this aim, wavelet analysis is acknowledged as the most effective method for de-noising non-stationary thermal signals [50]. By using the multi-resolution and self-similarity characteristics of wavelet analysis, the pseudo-white noise in non-stationary thermal signals can be eliminated.

Regarding point (ii), Silipigni et al. [19] presented different de-trending algorithms and polynomial functions for LED-stimulated PuCT application. Their proposed non-linear fitting function is here used. Fig.9 (a) shows the denoised thermal signal together with non-linear fitting function obtained for a single pixel, whilst Fig.9 (b) depicts the same signal after step-heating component removal, thus ready for PuC.

As discussed in Section 2.2, Fig.10 shows examples of the impulse responses obtained for a single pixel after PuC, hence obtained by convolving the signal depicted in Fig.9 (b) with the matched filter $\Psi(t)$, both for a BC retrieved raw signal and for a BC de-trended and denoised raw signal. It can be noticed that the signal maximin amplitude is reduced when applying denoising due to the elimination of non-stationary thermal noise, but the smoothness of impulse response after pulse compression is increased with respect to the raw signal. Fig.10 depicts a sample impulse response of a single pixel, it can be observed that the level of the sidelobe compared to the mainlobe maximum amplitude is ~0.4. This may affect the process of the feature extraction performance. Therefore, as explained in Section 2.3, the signal has been truncated from 0 to 200 frames of the corresponding $T_h$. 

Fig.8 Schematic diagram of SUT: (a) plan view, (b) cross section view
4.2 Delaminated area location by Kernel-PCA

As illustrated in block 4 of Fig. 1, the K-PCA techniques is applied to enhance the delaminated area. In this section, detailed implementation will be introduced.

The impulse response $\tilde{h}(t)$ is a sequence of 1500 frames, i.e. 30 seconds corresponding to the whole $T_h$. However, when it comes to visualize the delamination, most of the frames contribute little to the defect location. To solve this problem, the K-PCA method described in section 2.3 is applied to find and learn the mutual relation of impulse response in individual pixels. Thus, the pixelwise-retrieved $\tilde{h}(t)$’s are embedded into a suitable high-dimensional feature space through Gaussian kernel function. In addition, the kernel method is also an efficient way to imply the nonlinear characteristics of the raw data.

Fig.11 shows the extracted thermal pattern from the raw data (threshold). It is noted that first thermal pattern projected by PC1 summarizes the overall heating phenomena during

![Fig. 9 Computation of de-trended signal for PuC: (a) BC raw data and non-linear fitting function; (b) De-trended signal](image)

![Fig. 10 Comparison of single pixel raw data impulse response and denoised impulse response](image)
experiment because the heating is conducted on one side of rectangular coil, which generates linear heating. The sensitivity of pattern 1 for visualizing defect is heavily reduced for increased delamination depth. This is because pattern 1 contains most of information about heating pattern, which might cover up the faithful defect information. It is observed that patterns 2 and 3 projected by PC2 and PC3 respectfully obtain opposite profile or weighting for delamination area. Pattern 2 generally presents the delamination in lower contrast while pattern 3 shows higher contrast compared to the surrounding area. This is because the eigenvectors extracted were supposed to be orthogonal with each other in kernel space $\phi$. The indicated relationship between pattern 2 and pattern 3 can enhance the detectability in delamination area through logic operation, which is shown in Fig.12. In addition, since the largest electric and thermal conductivity values are along the fiber orientation, the delamination as a thermal barrier, hinders the heat diffusion mainly in $0^\circ$ and $90^\circ$ directions, which makes the delamination edges hotter and the delamination region colder. As a result, the delamination and its edge have a large contrast in the thermal pattern 1. Based on this fact, the enhanced thermal pattern of the nine defects are presented in Fig.13, where the achieved higher contrast shows the profile of delamination. Compared to the results in [19], where defect #9 was not observable under flash thermography and LED-stimulated PuCT, the induced eddy current can still penetrate into 2.30 mm depth to generate detectable IR signature of the deepest delamination. Defect SNR is reduced after D5, where the square shape of delamination profile cannot be identified. However, the delaminated area can still be characterized by fiber structure in $0^\circ$ and $90^\circ$ from D6~D9 since induced eddy currents are parallel to $0^\circ$ and $90^\circ$, which have the largest electrical conductivity and thermal conductivity in SUT thus generating abnormal thermal wave with diffusion length $\mu$ longer than the delamination depth $d$.

Generally, artificial delamination in CFRP has been demonstrated to exhibit different patterns by K-PCA method. The enhanced pattern emphasizes the defect with a larger contrast in comparison to the sound regions and provides a guide on how to select the proper pixels or regions of impulse response to quantitively evaluate the different depths of delamination. In the Sections 4.3 and 4.4, the impulse response retrieved at the most abnormal pixels area are investigated for feature extraction.
Fig. 11 First three extracted thermal patterns: (a) D1, D2, D3, (b) D4, D5, D6, (c) D7, D8, D9
4.3 Crossing point feature analysis

As discussed in section 4.2, the delamination ranging from 0.46 mm to 2.30 mm of depth can be visualized by enhanced thermal pattern method based on the impulse response. Moreover, to determine the delamination depth, the phase contrast between defected and non-defected areas can be exploited, by comparison of the obtained impulse responses based on PT theory [51]. The defected areas are detected and selected by KPCA as shown in Fig. 14 in line with the sample introduction in the Fig. 8.

Each defected area and non-defected area are formed by five lines of data in the center of higher contrast and lower contrast based on enhanced pattern. Based on the selected area, the comparison between impulse responses of defected and non-defected areas are presented in the plot series of Fig. 15. It can be noted that the impulse response curves behave similarly on the general trend for both the defective and the sound areas. However, the defective area is cooling slower due to the thermal diffusivity, which means the material ability to exchange heat with its surroundings has become worse with the increase in depth. The deeper the delamination, the worse is the ability to exchange heat with non-defective area. Results showed in Fig. 17 demonstrates that the impulse response amplitude is less sensitive than the phase change of crossing point of defective and non-defective area. Thus, it is observed that the position of the first crossing point of impulse responses of defected and non-defected areas has a monotonic relationship with delamination depth, as shown in Fig. 15 (labelled area) and Fig. 16. This can serve as an excellent feature to quantify the delamination depth. From Fig. 16, it can be noted that the feature based on the crossing point value follows a linear trend if three defects in a row over the SUT are considered, e.g. D1-D3 or D6-D9, which is due to the linear coil used in this experiment. In fact, the experimental conditions can be considered the same if defects are on the same line. Better results could be possibly obtained by achieving a more uniform heating through optimizing coil shape.

However, after defect 6, the crossing pattern of defected area and non-defected area has been disturbed by noise (see Fig. 15 (c)). Moreover, extra crossing points are observed in D7, continuous equal value of defected and non-defected areas in D8 and initial disturbed crossing point in D9 are caused by the low SNR of original signal. Thus, despite the effectiveness of the denoised approach applied in this work, the clear information of defect is still challenging to be extracted in D7~D9.
To validate this crossing point feature of impulse responses, the experiments were conducted again under reflection modes. The process of feature extraction for transmission and reflection modes is the same as illustrated in the Fig.4. It is observed in Fig.16 and Fig.17 (b) that the proposed features have monotonic relationships with delamination depth in reflection mode. Furthermore, the proposed feature in reflection mode holds better linearity and sensitivity as shown in Fig.17 (b) and better stability (less standard deviation error) as in Fig.16 (b) than transmission mode. In addition, compared with impulse responses in transmission mode in Fig.15, the response curves of the delaminated and the non-delaminated areas in reflection mode becomes divergent. These differences can also be investigated in the future.

To summarize, the proposed crossing point feature was validated in both transmission and reflection modes so it can be concluded that the proposed feature can be used for quantifying CFRP delamination depth.

**Fig. 14** Selected damaged area and non-damaged area based on KPCA enhanced pattern

**Fig. 15** Crossing point feature obtained from mean value of selected impulse responses in transmission mode
4.4 Skewness feature analysis

Based on the mathematical definition of skewness, this feature can be used to quantify the asymmetry of the considered data. In this section, the skewness is calculated on the major part of impulse response (first 200 frames of $T_h$ period). It is observed that positive skewness values are found for impulse responses as depicted in Fig.18. In Fig.18 (a), the skewness of data in transmission mode shows monotonic relationship with delamination depth because the impulse response curves of 9 defects are becoming more symmetrical along with the increase of delamination depth. However, in reflection mode, Fig.18 (b), this relationship becomes less monotonic than in transmission mode, which might be due to the texture influence on the selection of abnormal pixels. As a matter of fact, in reflection mode the IR camera is much
closer to the coil than the transmission mode to maintain the same lift-off in two different modes. Thus, the fiber texture contribute in reflection mode is more evident than in transmission mode. Fig. 19 presents the enhanced pattern of defect #1 in transmission mode and reflection mode. It is observed that fiber structure in reflection mode is more obvious than the transmission mode, which proves the idea that texture influence is more significant in reflection mode. The crossing point performance is also good in reflection mode, even with surface texture influence as illustrated in Fig. 17 (b).

Overall, the skewness of extracted impulse response can help characterize the delamination depth because of its monotonic relationship with delamination depth.

Fig. 18 Error bar plot of the skewness features in different modes: (a) transmission mode, (b) reflection mode

Fig. 19 Enhanced pattern of defect #1: (a) transmission mode, (b) reflection mode

5. Conclusion and future work
In this work, ECPuCT has been presented for characterization of delamination depth in CFRP laminates using different features comparison and validation including crossing point and skewness. The proposed features were verified through experimental studies under both transmission and reflection modes. The conclusions are as follows:

1) The K-PCA method can well extract the meaningful pattern in the impulse response behavior as time elapses, helping thus in locating the delamination areas effectively. It was observed that the method can reveal the spatial pattern, which corresponds to the defect with enhanced contrast, hence improving defect detectability and noise reduction capability.

2) The proposed crossing point feature is extracted based on the crossing point of impulse response from defective and non-defective areas previously discriminated by the K-PCA method. This feature has monotonic trend in both transmission and reflection modes with delamination depths. The feature performance in term of linearity is better in reflection mode than in transmission mode.

3) Skewness feature of impulse response is also investigated. It illustrates the monotonic relationship with delamination depths in transmission mode as well. However, the
monotonic relationship does not keep with delamination depths in reflection mode due to the influence of the texture structure. Compared with other features’ performance in reflection mode, the feature of crossing point demonstrates more robustness against texture to ensure the stability in reflection mode.

The future work will investigate:
1) The use of other coded signals and the optimization of Barker code single bit length for ECPuCT and further quantitative evaluation of texture influence on the proposed features.
2) The application of the proposed features of depth characterization on thermographic tomography and further investigation of different range of impulse responses for characterizing eddy current and thermal diffusion for evaluation of low energy impact damage and fiber breakage in composites materials.

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