CALCULATIONS OF THE ISOSCALAR GIANT MONOPOLE RESONANCE WITHIN THE SELF-CONSISTENT RPA AND ITS EXTENSIONS

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The strength distributions of the isoscalar giant monopole resonance have been calculated in $^{16}$O, $^{40}$Ca, $^{90}$Zr, $^{112-124}$Sn, $^{144}$Sm, and $^{208}$Pb nuclei within the self-consistent random phase approximation and its extensions which include pairing correlations and quasiparticle-phonon coupling. The results are compared with the available experimental data. The problem of the nuclear matter incompressibility is discussed.

Theoretical description of the isoscalar giant monopole resonance (ISGMR) is an important issue, first of all, because its energy is closely related to the value of the incompressibility modulus of infinite nuclear matter (INM) $K_\infty$ (see [1, 2]), which in turn is a universal characteristic of the effective nuclear forces. The most widely used method of evaluating $K_\infty$ is based on the self-consistent Hartree-Fock (HF) or random phase approximation (RPA) calculations of the mean energies of the ISGMR using effective Skyrme or Gogny forces (see, e.g., Refs. [1, 2, 3, 4, 5]). Because $K_\infty$ can be calculated from the known parameters of the given force, its value is estimated as the one corresponding to the force that gives the best description of the experimental energies. The non-relativistic estimates obtained in such a way lead to the value $K_\infty = 210 \pm 30$ MeV (see, e.g., Refs. [2, 3]), though the recent results testify to the upper limit of this estimate (see [4, 5]).

However, neither the HF approximation nor the RPA can provide full description of the experimental data. In particular, they cannot reproduce the total width $\Gamma$ of the giant resonance, since in these models the mechanism responsible for the formation of the spreading width $\Gamma^\dagger$ is absent. At the same time, it is well known that the spreading width is a considerable part of $\Gamma$. In the present work we report the results of the ISGMR calculations within three models: (i) the RPA; (ii) the quasiparticle RPA (QRPA); (iii) the quasiparticle time blocking approximation (QTBA, see [6, 7]) which is an extension of the QRPA including quasiparticle-phonon coupling (QPC). The QPC provides the necessary mechanism producing the spreading width in the QTBA. The pairing correlations are taken into account both in the QRPA and in the QTBA.
The basic equation of our approach is the equation for the effective response function $R^{\text{eff}}(\omega)$. It has the same form both in the (Q)RPA and in the QTBA. In the shorthand notations it reads (we will follow notations of Ref. [7])

$$R^{\text{eff}}(\omega) = A(\omega) - A(\omega) F^{R} R^{\text{eff}}(\omega),$$  \hspace{1cm} (1)

where $A(\omega)$ is a correlated propagator and $F$ is an amplitude of the effective residual interaction. In the present work we use the version of the QTBA in which the ground-state correlations caused by the QPC are neglected. In this case the correlated propagator $A(\omega)$ is defined by the equation

$$A(\omega) = \tilde{A}(\omega) - \tilde{A}(\omega) \bar{\Phi}(\omega) A(\omega),$$  \hspace{1cm} (2)

where $\tilde{A}(\omega)$ is the uncorrelated QRPA propagator,

$$\bar{\Phi}(\omega) = \Phi^{(\text{res})}(\omega) - \Phi^{(\text{res})}(0),$$  \hspace{1cm} (3)

and $\Phi^{(\text{res})}(\omega)$ is a resonant part of the interaction amplitude responsible for the QPC in our model (see Refs. [6, 7] for details). In the case of the (Q)RPA, the amplitude $\Phi^{(\text{res})}(\omega)$ is set equal to zero, and $A(\omega)$ reduces to the uncorrelated propagator $\tilde{A}(\omega)$. The dynamical pairing effects (particle-particle channel contributions) are taken into account both in the QRPA and in the QTBA. This enables one to eliminate the $0^+$ spurious states on the QRPA level. The problem of the $0^+$ spurious states in the QTBA is solved with the help of a combination of the so-called subtraction procedure (see Eq. (3) and Refs. [6, 7] for details) and the projection technique described in [8].

The strength function of the ISGMR $S(E)$ is determined by $R^{\text{eff}}(\omega)$ via the formulas

$$S(E) = -\frac{1}{\pi} \text{Im} \Pi(E + i\Delta),$$  \hspace{1cm} (4)

$$\Pi(\omega) = -\frac{1}{2} \text{Tr} \left( (eV^0)^\dagger R^{\text{eff}}(\omega) (eV^0) \right),$$  \hspace{1cm} (5)

where $\Pi(\omega)$ is the nuclear polarizability, $E$ is an excitation energy, $\Delta$ is a smearing parameter, $V^0$ is an external field, and $e$ is an effective charge operator. In the case of the isoscalar $0^+$ excitations the one-body operator $eV^0$ is proportional to the identity matrices both in the spin and in the isospin indices. Its radial dependence is taken in our calculations in the form $eV^0 = r^2$. The smearing parameter is taken to be equal to 500 keV in all the calculations presented here.

We used a self-consistent calculation scheme based on the HF and Bardeen-Cooper-Schrieffer (HF+BCS) approximation. The details of this scheme are described in Ref. [9]. Within the RPA the self-consistency is full. The single-particle continuum is also exactly included on the RPA level. The self-consistent mean field and the effective interaction (including the spin-orbital and the Coulomb contributions in both quantities) are derived from the Skyrme energy functional.
the calculations, two Skyrme force parametrizations with the nucleon effective mass \( m^* = m \) were used (see Ref. [10]): T5 force with \( K_\infty = 202 \text{ MeV} \) and T6 force with \( K_\infty = 236 \text{ MeV} \). The ISGMR calculations were performed in \(^{16}\text{O}, ^{40}\text{Ca}, \text{ and } ^{90}\text{Zr}\) nuclei, in the chain of the Sn isotopes, and in \(^{144}\text{Sm}\) and \(^{208}\text{Pb}\) nuclei.

The results for the ISGMR strength distributions in the even-\( A \) \( ^{112-124}\text{Sn}\) isotopes are presented in Fig. 1 and in Table 1. The mean energies of the ISGMR drawn in the tables are defined via the ratios of the energy-weighted moments \( m_k \) determined as

\[
m_k = \int_{E_1}^{E_2} E^k S(E) \, dE.
\]

The energy interval limited by \( E_1 = 10.5 \text{ MeV} \) and \( E_2 = 20.5 \text{ MeV} \) was taken the same as in Ref. [11], where the experimental data on the strength distributions of the ISGMR in the tin isotopes were reported. The peak energies \( E_{\text{GMR}} \) and the widths \( \Gamma \) of the ISGMR were obtained from the Lorentzian fit of the calculated functions \( S(E) \). As can be seen from the Table 1, the agreement of the theoretical results with the experimental mean and peak energies in the case of the T5 Skyrme force is fairly good both in the QRPA and in the QTBA. The fact that the mean and peak energies obtained in the QRPA and in the QTBA are very close to each other is explained by the subtraction procedure used in our calculations (see Eq. (3) and Ref. [7] for the discussion). The main reason of the agreement with the experiment in this case is comparatively low value of the incompressibility modulus of INM \( (K_\infty = 202 \text{ MeV}) \) produced by the T5 Skyrme-force parametrization. The other parametrizations with \( K_\infty \) around 240 MeV give too large mean energies of the ISGMR in the considered tin isotopes as compared with the experiment.

For comparison, in Table 1 we draw the QRPA results obtained with the T6 Skyrme force \( (K_\infty = 236 \text{ MeV}) \). As can be seen, the T6 peak energies \( E_{\text{GMR}} \) are greater than the experimental values for the tin isotopes by 1.2–1.9 MeV. This fact agrees with the results of Ref. [12] where it was obtained that the relativistic RPA calculations based on the force with \( K_\infty = 230 \text{ MeV} \) consistently overestimate the centroid energies of the ISGMR in the same tin isotopes.

In Table 2, the (Q)RPA and QTBA results for \(^{16}\text{O}, ^{40}\text{Ca}, ^{90}\text{Zr}, ^{144}\text{Sm}, \text{ and } ^{208}\text{Pb}\) nuclei are listed in comparison with the available ISGMR data. As can be seen from this table, the T5 Skyrme force leads to a better description of the experiment in the light nuclei \(^{16}\text{O}\) and \(^{40}\text{Ca}\). The experimental value of the ISGMR peak energy in \(^{90}\text{Zr}\) obtained by the RCNP (Osaka University, Ref. [17]) and the value \( m_1/m_0 \) for this nucleus obtained by the Gaussian fit in the TAMU experiment (Texas A\&M University, Ref. [15]) are also fairly well reproduced by the calculations with the T5 Skyrme force. The other experimental data for \(^{90}\text{Zr}\) and \(^{144}\text{Sm}\) nuclei lie between the values calculated with the T5 and T6 forces.

It is worth noting that the value \( K_\infty = 202 \text{ MeV} \) corresponding to the T5 Skyrme force lies within the interval \( 210 \pm 30 \text{ MeV} \) which was considered for a long time as the non-relativistic estimate for this quantity. The recent results [4, 5] inferring \( K_\infty \) to be 230–240 MeV were obtained within the RPA and the constrained
Figure 1: Isoscalar giant monopole resonance in the even-\(A^{\,112-124}\) Sn isotopes calculated within the QRPA (dashed line) and the QTBA (solid line) using T5 Skyrme force. The smearing parameter \(\Delta\) is equal to 500 keV. Experimental data (solid squares) are taken from Ref. [11].
Table 1: Mean energies and Lorentzian-fit parameters for the ISGMR strength distributions in the even-$^A$\textsuperscript{112−124}Sn isotopes. Theoretical results are obtained within the QRPA and the QTBA using T5 and T6 Skyrme forces (indicated in parentheses). The mean energies are calculated for 10.5–20.5 MeV energy interval. Experimental values are taken from Ref. [11] (RCNP, Osaka University).

| Method  | $\sqrt{m_1/m_{-1}}$ (MeV) | $m_1/m_0$ (MeV) | $\sqrt{m_3/m_1}$ (MeV) | $E_{\text{GMR}}$ (MeV) | $\Gamma$ (MeV) |
|---------|--------------------------|----------------|------------------------|-------------------|---------------|
| $^{112}$Sn | QRPA (T6) | 17.0 | 17.1 | 17.3 | 17.3 | 1.9 |
|          | QRPA (T5) | 15.8 | 15.9 | 16.1 | 15.9 | 1.8 |
|          | QTBA (T5) | 15.7 | 15.8 | 16.2 | 15.8 | 3.7 |
|          | Exp. | 16.1^{+0.1}_{-0.1} | 16.2^{+0.1}_{-0.1} | 16.7^{+0.2}_{-0.2} | 16.1^{+0.1}_{-0.1} | 4.0^{+0.4}_{-0.4} |
| $^{114}$Sn | QRPA (T6) | 16.9 | 17.0 | 17.2 | 17.3 | 2.0 |
|          | QRPA (T5) | 15.7 | 15.8 | 16.0 | 15.8 | 1.8 |
|          | QTBA (T5) | 15.6 | 15.7 | 16.1 | 15.7 | 3.7 |
|          | Exp. | 15.9^{+0.1}_{-0.1} | 16.1^{+0.1}_{-0.1} | 16.5^{+0.2}_{-0.2} | 15.9^{+0.1}_{-0.1} | 4.1^{+0.4}_{-0.4} |
| $^{116}$Sn | QRPA (T6) | 16.8 | 16.9 | 17.1 | 17.2 | 2.1 |
|          | QRPA (T5) | 15.6 | 15.6 | 15.9 | 15.7 | 1.9 |
|          | QTBA (T5) | 15.5 | 15.6 | 16.0 | 15.6 | 3.8 |
|          | Exp. | 15.7^{+0.1}_{-0.1} | 15.8^{+0.1}_{-0.1} | 16.3^{+0.2}_{-0.2} | 15.8^{+0.1}_{-0.1} | 4.1^{+0.3}_{-0.3} |
| $^{118}$Sn | QRPA (T6) | 16.6 | 16.7 | 17.0 | 17.1 | 2.1 |
|          | QRPA (T5) | 15.4 | 15.5 | 15.8 | 15.6 | 2.0 |
|          | QTBA (T5) | 15.4 | 15.5 | 15.9 | 15.5 | 3.9 |
|          | Exp. | 15.6^{+0.1}_{-0.1} | 15.8^{+0.1}_{-0.1} | 16.3^{+0.1}_{-0.1} | 15.6^{+0.1}_{-0.1} | 4.3^{+0.4}_{-0.4} |
| $^{120}$Sn | QRPA (T6) | 16.5 | 16.6 | 16.9 | 17.0 | 2.2 |
|          | QRPA (T5) | 15.3 | 15.4 | 15.7 | 15.5 | 2.1 |
|          | QTBA (T5) | 15.3 | 15.4 | 15.8 | 15.3 | 3.9 |
|          | Exp. | 15.5^{+0.1}_{-0.1} | 15.7^{+0.1}_{-0.1} | 16.3^{+0.2}_{-0.2} | 15.4^{+0.2}_{-0.2} | 4.9^{+0.5}_{-0.5} |
| $^{122}$Sn | QRPA (T6) | 16.4 | 16.5 | 16.8 | 16.9 | 2.3 |
|          | QRPA (T5) | 15.2 | 15.3 | 15.5 | 15.4 | 2.1 |
|          | QTBA (T5) | 15.1 | 15.3 | 15.7 | 15.2 | 3.8 |
|          | Exp. | 15.2^{+0.1}_{-0.1} | 15.4^{+0.1}_{-0.1} | 15.9^{+0.2}_{-0.2} | 15.0^{+0.2}_{-0.2} | 4.4^{+0.4}_{-0.4} |
| $^{124}$Sn | QRPA (T6) | 16.2 | 16.4 | 16.7 | 16.7 | 2.3 |
|          | QRPA (T5) | 15.0 | 15.1 | 15.4 | 15.2 | 2.2 |
|          | QTBA (T5) | 15.0 | 15.2 | 15.5 | 15.1 | 3.8 |
|          | Exp. | 15.1^{+0.1}_{-0.1} | 15.3^{+0.1}_{-0.1} | 15.8^{+0.1}_{-0.1} | 14.8^{+0.2}_{-0.2} | 4.5^{+0.5}_{-0.5} |
Table 2: The same as in Table 1 but for $^{16}\text{O}$, $^{40}\text{Ca}$, $^{90}\text{Zr}$, $^{144}\text{Sm}$, and $^{208}\text{Pb}$ nuclei. The theoretical mean energies are obtained for the following energy intervals: 11–40 MeV in $^{16}\text{O}$, 10–55 MeV in $^{40}\text{Ca}$, and 5–25 MeV in $^{90}\text{Zr}$, $^{144}\text{Sm}$, and $^{208}\text{Pb}$. Experimental data are taken from Refs. [13, 14, 15, 16] (TAMU, Texas A&M University) and [17, 18] (RCNP, Osaka University). The data from Ref. [15] for $^{90}\text{Zr}$ denoted as $[15]^a$ and $[15]^b$ correspond to the slice analysis and to the Gaussian fit, respectively.

| Method       | $\sqrt{m_1/m_{-1}}$ (MeV) | $m_1/m_0$ (MeV) | $\sqrt{m_3/m_1}$ (MeV) | $E_{\text{GMR}}$ (MeV) | $\Gamma$ (MeV) |
|--------------|-----------------------------|-----------------|------------------------|-------------------------|---------------|
| $^{16}\text{O}$ RPA (T6) | 22.7                        | 23.3            | 25.1                   | 22.0                    | 10.3          |
|              RPA (T5)       | 21.3                        | 21.8            | 23.4                   | 20.5                    | 7.2           |
|              Exp. [13]     | 19.63$^{+0.38}_{-0.38}$     | 21.13$^{+0.49}_{-0.49}$ | 24.89$^{+0.59}_{-0.59}$ | 8.76$^{+1.82}_{-1.82}$ |
| $^{40}\text{Ca}$ RPA (T6) | 21.2                        | 21.6            | 23.0                   | 21.6                    | 4.8           |
|              RPA (T5)       | 19.7                        | 19.9            | 21.1                   | 19.7                    | 4.0           |
|              Exp. [14]     | 19.18$^{+0.37}_{-0.37}$     |                 |                        |                         | 4.88$^{+0.57}_{-0.57}$ |
| $^{90}\text{Zr}$ QRPA (T6) | 18.0                        | 18.2            | 18.6                   | 18.0                    | 3.0           |
|              QTBA (T6)     | 18.0                        | 18.2            | 18.7                   | 18.0                    | 3.8           |
|              QRPA (T5)     | 16.6                        | 16.8            | 17.2                   | 16.5                    | 2.0           |
|              QTBA (T5)     | 16.6                        | 16.8            | 17.3                   | 16.5                    | 2.6           |
|              Exp. [15]$^a$ | 17.81$^{+0.35}_{-0.35}$     | 17.89$^{+0.20}_{-0.20}$ |                   |                         |               |
|              Exp. [15]$^b$ |                             |                 |                        |                         |               |
|              Exp. [17]     |                             |                 |                        |                         |               |
| $^{144}\text{Sm}$ QRPA (T6) | 15.8                        | 16.0            | 16.4                   | 15.8                    | 2.0           |
|              QTBA (T6)     | 15.8                        | 16.1            | 16.7                   | 15.8                    | 3.0           |
|              QRPA (T5)     | 14.6                        | 14.7            | 15.1                   | 14.5                    | 1.5           |
|              QTBA (T5)     | 14.6                        | 14.8            | 15.4                   | 14.4                    | 2.5           |
|              Exp. [16]     | 15.40$^{+0.30}_{-0.30}$     |                 |                        |                         | 3.40$^{+0.20}_{-0.20}$ |
|              Exp. [18]     |                             |                 |                        |                         | 15.30$^{+0.11}_{-0.12}$ | 3.71$^{+0.12}_{-0.63}$ |
| $^{208}\text{Pb}$ RPA (T6) | 13.8                        | 14.0            | 14.5                   | 13.9                    | 1.9           |
|              QTBA (T6)     | 13.8                        | 14.1            | 14.8                   | 13.9                    | 3.2           |
|              RPA (T5)      | 12.6                        | 12.7            | 13.2                   | 12.6                    | 1.6           |
|              QTBA (T5)     | 12.6                        | 12.8            | 13.5                   | 12.5                    | 2.8           |
|              Exp. [16]     | 13.96$^{+0.20}_{-0.20}$     |                 |                        |                         | 2.88$^{+0.20}_{-0.20}$ |
|              Exp. [17]     |                             |                 |                        |                         | 13.4$^{+0.2}_{-0.2}$ | 4.0$^{+0.4}_{-0.4}$ |

HF method on the base of the experimental data in fact only for the one nucleus $^{208}\text{Pb}$. The mean energy $m_1/m_0$ of the ISGMR in $^{208}\text{Pb}$ obtained in the TAMU experiment [16] is also nicely reproduced in our calculations when the T6 force with
$K_\infty = 236$ MeV is used. On the other hand, the T5 force gives the QTBA value $m_1/m_0$ for $^{208}$Pb which is lesser by 1.2 MeV as compared with this experiment. Note, however, that the ISGMR data even for the well-studied nucleus $^{208}$Pb are not so far quite unambiguous. In particular, the experimental value of the ISGMR peak energy in $^{208}$Pb measured in the RCNP experiment [17] is lesser by 0.6 MeV as compared with the value $m_1/m_0$ from Ref. [16] and lies between the QTBA values of $E_{\text{GMR}}$ obtained with the T5 and T6 Skyrme forces.

In contrast to the mean energies, the (Q)RPA and the QTBA give substantially different values for the total width $\Gamma$ of the ISGMR. As was mentioned above, the reason is that the (Q)RPA does not produce the spreading width $\Gamma^\downarrow$, whereas in the QTBA it is formed due to the QPC effects. The fact that $\Gamma^\downarrow$ is a considerable part of $\Gamma$ is illustrated by the results listed in the tables: the (Q)RPA strongly underestimates the experimental values of the total width, while reasonably good agreement is achieved in the QTBA. The exception is the case of the light nuclei in which the resonance width is fairly well reproduced already within the RPA.

In conclusion, we have presented the results of the theoretical analysis of the ISGMR strength distributions in $^{16}$O, $^{40}$Ca, $^{90}$Zr, $^{112}$-124Sn, $^{144}$Sm, and $^{208}$Pb nuclei. The calculations were performed within the (Q)RPA and the QTBA which is an extension of the QRPA including quasiparticle-phonon coupling (QPC). We used calculational scheme based on the HF+BCS approximation which is fully self-consistent on the RPA level. In the calculations, two Skyrme force parametrizations were used. The T5 parametrization with comparatively low value of the incompressibility modulus of infinite nuclear matter ($K_\infty = 202$ MeV) allowed us to achieve good agreement with the experimental data for tin isotopes within the QTBA including resonance widths. However, this parametrization underestimates the experimental ISGMR mean energy for the $^{208}$Pb nucleus which is usually used in the fit of the Skyrme force parameters. On the other hand, the T6 Skyrme force with $K_\infty = 236$ MeV nicely reproduces the ISGMR mean energy for $^{208}$Pb but overestimates the energies for $^{112}$-124Sn isotopes by more than one MeV. For the light nuclei $^{16}$O and $^{40}$Ca, the T5 Skyrme force gives a better description of the experimental ISGMR mean energies as compared with the T6 force. The experimental data on the ISGMR energies in $^{90}$Zr and $^{144}$Sm nuclei lie between the values calculated by us with the T5 and T6 forces. On the whole, these results do not allow us to decrease the ambiguity in the value of $K_\infty$ as compared with the known estimate $K_\infty = 210 \pm 30$ MeV. However, our calculations confirm that an account of the QPC is necessary to describe the total width of the ISGMR.

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