Photon emission rates near the critical point in the linear sigma model

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Employing the linear sigma model, the effective masses of quasi-particle excitations are found to exhibit significant variations within the phase diagram, which has a critical point at non-zero chemical potential, where a first-order phase transition sets in. Soft-photon emission rates in lowest order display, for selected channels, a sensible dependence on the effective masses of the involved excitations and let us argue that they could map out the phase diagram.

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1. Introduction

Confinement and spontaneous symmetry breaking as well as their respective counterparts - deconfinement and chiral restoration - are central issues of QCD. Their mutual relationship is among the main questions investigated in heavy ion collisions (HICs). A particularly challenging task is the establishment of the QCD phase diagram in a region of temperature $T$ and baryo-chemical potential $\mu$ which is accessible in HICs. While the beam energy scan at RHIC and forthcoming accelerator/detector installations, e.g. at FAIR/CBM and NICA/MPD, aim at finding signatures of the onset of deconfinement as a first-order phase transition in a critical point (CP), QCD based [1,2] and QCD rooted [3] calculations try to quantify its coordinates. Instead of facing the sign problem of QCD at non-zero baryon density, one can resort to suitable models which display a CP at $(T_{CP}, \mu_{CP}) > (0,0)$ and a line of first-order phase transitions for $\mu > \mu_{CP}$ (cf. [4, 5] for recent surveys). By universality arguments, one can elucidate observables signaling the CP.

In the previous search for deconfinement effects in HICs, electromagnetic probes (cf. [6–8] for recent evaluations and further references) have been considered as promising since, by their penetrating nature, they monitor the full space-time evolution of matter in the course of HICs. Given the proximity of deconfinement and chiral restoration at $\mu/T \ll 1$, the dilepton spectra have been considered in [9, 10] as candidates for messengers of chiral restoration. It appeared that at the pseudo-critical temperature of $T_{pc} \sim 154\,\text{MeV}$ the dilepton emission rates of confined matter (hadrons) and deconfined matter (quarks and gluons) become degenerate - quite natural since $T_{pc}$ quantifies the cross over location at $\mu/T \ll 1$. This degeneracy can be named quark-hadron duality and has been employed [11–13] to verify a “thermal radiation” component besides hard initial yield and electromagnetic hadron final-state decays after the disassembly of the fireball in HICs. The approximate degeneracy of real-photon emission rates of confined and deconfined matter has been pointed out quite early [14] and can be used analogously to arrive at a consistent modeling of thermal radiation in HICs, either schematically [15, 16] or with many refinements [17–19].

The recent analysis in [17, 20], however, revealed that the calculated photon spectra fall short in comparison with data. The tension is caused, to some extent, by the consistency requirement of photon-$v_2$ and photon-$p_{\perp}$ systematics. According to [17,18], a solution is offered by the hypothesis of a “pseudo-critical enhancement” of the photon emission at $T_{pc} \pm \Delta T$ with $\Delta T = O(15\,\text{MeV})$. It is therefore tempting to look for arguments which could support the hypothesis launched there and, more general, to extend the consideration over the QCD phase diagram and to check whether the CP can have a distinguished impact on the photon emission rate.

2. Linear $\sigma$ model

We utilize here the linear sigma model (L$\sigma$M), which has been originally designed to model spontaneous chiral symmetry breaking [21] and has been later coupled to the fermionic sector. It is a special quark-meson model with the Lagrangian $\mathcal{L}_{L\sigma M} = \mathcal{L}_{\partial \psi} + \mathcal{L}_{\psi M} + \mathcal{L}_{\partial M} + \mathcal{L}_M + \mathcal{L}_{\text{b.f.}}$, where the kinetic terms $\mathcal{L}_{\partial \psi}$ and $\mathcal{L}_{\partial M}$ are supplemented by the $O(4)$ symmetric meson self-interaction $\mathcal{L}_M$, which refers to an $SU(2)_L \times SU(2)_R$ symmetry which, in combination with the symmetry breaker $\mathcal{L}_{\text{b.f.}} = H\sigma$, dynamically generates mass terms; the fermion-meson coupling of Yukawa type is encoded in $\mathcal{L}_{\psi M}$. The field content of $\mathcal{L}$ is a two component Fermion (light quark doublet
\(\psi\), an iso-vector (\(\vec{\pi}\)) and an iso-scalar (\(\sigma\)) meson. (The model can be extended to SU(3) and may include vector mesons [22] in the spirit of the gauged L\(\sigma\)M [23] or can be supplemented by some gluon dynamics encoded in the Polyakov loop [24] or a glueball condensate [25].) When including linearized meson field fluctuations, as in [26–28], the resulting phase diagram has, in fact, a line of first-order phase transitions (cf. solid curves in Fig. [2]), where the pressure as a function of \(T\) and \(\mu\) has a self-intersection defining \(T_c(\mu)\). The fine structure of the region, where the CP is located [28], is thought to reflect the restriction to linearized fluctuations. (For a better account of fluctuations within a FRG approach, cf. [29].)

The parameters in the Lagrangian are commonly fixed by requiring a coincidence of the dynamically generated meson quasi-particle masses in the vacuum \((T = \mu = 0)\) with the experimental values of pion, \(m^{\text{vac}}_{\pi} = 138\text{MeV}\), and sigma, \(m^{\text{vac}}_{\sigma} = 700\text{MeV}\), and the constituent quark mass, adjusted to one third of the nucleon mass, \(m^{\text{vac}}_{\psi} = 312\text{MeV}\). The remaining free parameter is determined by \(\langle \sigma \rangle_{\text{vac}} = f_{\pi}\). With these settings, the CP coordinates are \((T_{CP}, \mu_{CP}) \sim (74\text{MeV}, 278\text{MeV})\) (without the Fermion vacuum loop; for its impact cf. [30]). Since the sigma field in \(\mathcal{L}_{\sigma M}\) can be considered as an effective field which may be tentatively identified with \(f_0(600)\) leading to vacuum mass values of \(m^{\text{vac}}_{\sigma} = 400 - 800\text{MeV}\). It is instructive to study its impact on the phase diagram (cf. left panel of Fig. [1]). It turns out that the phase contour curves are shifted approximately linearly with \(m^{\text{vac}}_{\sigma}\). For an estimate we note \(\Delta T_{PC} \approx 0.12\Delta m_\sigma\) on the temperature axis. The CP is shifted approximately parallel to the \(\mu\) axis by about 40MeV per 100MeV change of \(m^{\text{vac}}_{\pi}\) in this mass region. The impact of \(m^{\text{vac}}_{\pi}\) is discussed extensively in [27]. We refrain here from a discussion of the phase structure under variations of all parameters at fixed \(T_{PC}\), which we define here as the curve, where the normalized heat capacity as a function of \(T\) at fixed \(\mu\) has a maximum - other definitions of the pseudo-critical temperature are conceivable. For further discussion of the phase diagram within effective chiral quark-meson models cf. [31–33].

Analogously to the mean field approximation [34] a crucial role is played by dynamically generated mass terms, which may be considered as quasi-particle masses \(m_{\psi, \pi, \sigma}\) (cf. Fig. [2]) of thermal excitations of the \(\psi, \pi, \sigma\) and fields (for details see [35]). Prominent features are (i) degeneracy of \(m_\pi\) and \(m_\sigma\) at temperatures larger than \(T_{PC}(\mu)\) or \(T_c(\mu)\), respectively, (ii) a rapid dropping of \(m_\psi\) at \(T = T_c(\mu)\) and a mild dropping at \(T \sim T_{PC}(\mu)\) and (iii) a global minimum of \(m_\sigma\) at \((T_{CP}, \mu_{CP})\) (for the rationale of the softening of the \(\sigma\)-mode, cf., e.g., [36–38] and for the impact on di-photon spectra [39, 40]).

It is remarkable that the mass ordering changes over the \(T\)-\(\mu\) plane, see Fig. [1] (right panel). The delineation of \(2m_q > m_{\pi, \sigma}\) vs. \(2m_q < m_{\pi, \sigma}\) coincides with \(T_c(\mu)\). There is a narrow valley, wherein \(m_\sigma < 2m_q < m_\pi\) separating \(2m_q > m_{\pi, \sigma}\) vs. \(2m_q < m_{\pi, \sigma}\) regions. This and the other delineation curves have no direct relation to \(T_c(\mu)\) or \(T_{PC}(\mu)\).

### 3. Photon emission rates

In a phenomenological approach and as a first exploratory step one can consider the above mentioned quasi-particle masses as masses of the quanta entering the respective dispersion relations \(E^2_{\psi, \pi, \sigma} = \vec{p}^2 + m^2_{\psi, \pi, \sigma}\), which in turn show up in the thermal occupation functions (cf. appendix B in [29]). Due to the strong variations of these masses over the phase diagram (cf. Fig. [3]), one can expect also a non-trivial pattern of the real-photon emission rate (see figure 2 in [35]).
Figure 1: Left panel: Phase structure of the LσM for various values of the sigma mass parameter $m_{\sigma}^{\text{vac}} = 400, 500, 600, 700$ and $800 \text{ MeV}$ (bottom to top). The solid curves depict first-order phase transition lines and the dotted curves are an estimate for a pseudo-critical temperature $T_{\text{pc}}(\mu)$. Both curves meet at the CP (dots). Right panel: Relations of the effective masses $m_{\omega,\pi,\sigma}$ over the phase plane (for $m_{\sigma}^{\text{vac}} = 700 \text{ MeV}$, with phase structure as in left panel).

Figure 2: Quark (blue solid curve), sigma (red dashed curve) and pion (green dotted curve) effective masses as a function of the quark chemical potential $\mu$ for temperatures slightly below (left panel), at (middle panel) and slightly above (right panel) the critical temperature $T_{\text{CP}}$. The position of the critical chemical potential $\mu_{\text{CP}}$ is depicted by the thin vertical line in the middle panel.

Leaving a theoretically sound approach from Wightman functions to imaginary part of the retarded photon propagator to kinetic theory expressions from cutting rules for separate work, we employ the phenomenologically anticipated kinetic approach by estimating the rates via

$$
\omega \frac{d^4N}{d^4x dk^3} = C \int \frac{d^3p_1}{2p_1^0} \frac{d^3p_2}{2p_2^0} \frac{d^3p_3}{2p_3^0} f_1(p_1)f_2(p_2)(1 \pm f_3(p_3)) |M_{12 \rightarrow 3\gamma}|^2 \delta^{(4)}(p_1 + p_2 - p_3 - k),
$$

with $C = (2(2\pi)^3)^{-1}$, i.e. we account for lowest-order tree-level $2 \rightarrow 2$ processes $1 + 2 \rightarrow 3 + \gamma$, where the photons are minimally coupled to $\mathcal{L}_{\text{LσM}}$ according to [41]. These are annihilations $\psi_i + \bar{\psi}_j \rightarrow M + \gamma$ and Compton processes $\psi_i + M \rightarrow \psi_j + \gamma$ and $\bar{\psi}_i + M \rightarrow \bar{\psi}_j + \gamma$, respectively, with $i, j \in \{u, d\}$ and $M \in \{\pi^0, \pi^\pm, \sigma\}$ being the respective meson(s) fulfilling charge conservation depending on the choice of $i, j$. (Clearly, this list of reactions is by far not exhaustive when having in mind hadronic sources in general. For instance, in [42] the non-linear $\sigma$ model with vector and axial-vector mesons has been used to investigate real-photon emission rates from hadron sources. In [43], the channel $\pi^+\pi^- \rightarrow \sigma/\rho \rightarrow \pi^+\pi^-\gamma$ has been identified as important for soft photons. This and many more channels should be considered when attempting a comprehensive rate estimate.)
The matrix elements for Compton and annihilation processes are related by crossing symmetries. The evaluation of (3.1) by means of the \( \delta^{(4)} \) and exploiting the cylinder symmetry in the center of mass frame of the reaction leaves four integrals [44, 45] to be done numerically.

4. Photon spectra

An instructive form of (3.1) can be derived by resorting to the Boltzmann approximation:

\[
\frac{d^3N}{dk^3} \approx \tilde{C}e^{\varepsilon \mu / T} \int_{s_0}^\infty ds \frac{\tilde{\sigma}(s)}{s - m_3^2} e^{-F(s)/T}
\]

(4.1)

with \( \tilde{C} = T/(32\omega(2\pi)^6) \), \( \tilde{\sigma}(s) = \int_{t^o} dt |M_{12-3\gamma}|^2 \), \( t_{\pm} = m_1^2 - \frac{\lambda}{2s} ((s + m_1^2 - m_2^2) + \sqrt{\lambda(s, m_1^2, m_2^2)}) \), \( \lambda(x, y, z) = x^2 + y^2 + z^2 - 2xy - 2xz - 2yz \), \( F(s) = (s - m_3^2)/(4\omega) + (s\omega)/(s - m_3^2) \) and \( \sqrt{s_0} = \max\{m_1 + m_2, m_3\} \). The variable \( \varepsilon \) discriminates between three reaction types under consideration: annihilation (\( \varepsilon = 0 \), Compton scattering at quarks (\( \varepsilon = +1 \)) and Compton scattering at antiquarks (\( \varepsilon = -1 \)). For disentangling effects of the phase space distributions \( f_{1-3} \), in particular the role of the involved quasi-particle masses, and matrix elements \( M_{12-3\gamma} \) encoded in \( \tilde{\sigma}(s) \) let us analyze the function \( F \). Two cases are to be distinguished: (i) If the position of the minimum of \( F \) w.r.t. \( s \), \( s_1 = m_1^2 + 2\omega m_3 \), lies within the range of integration, i.e. \( s_0 < s_1 \), a Taylor expansion \( F(s) = F(s_1) + 1/2 \cdot F''(s_1) \cdot (s - s_1)^2 + \mathcal{O}((s - s_1)^3) \) is in order and the exponential in (4.1) can be replaced by a Gaussian with width \( \sqrt{4m_3\omega^2T} \) and height \( \exp\{-F(s_1)/T\} \), making the exponential thermal suppression apparent. (ii) If \( s_1 < s_0 \), a Taylor expansion \( F(s) = F(s_0) + F'(s_0) \cdot (s - s_0) + \mathcal{O}((s - s_0)^2) \) yields a \( s \) independent suppression factor \( \exp\{-F(s_0)/T\} \) that develops a maximum w.r.t. \( \omega \) at \( \omega_p = (s_0 - m_3^2)/(2\sqrt{s_0}) \), meaning the spectrum displays a peak at \( \omega_p > 0 \). Whether it appears is thus controlled by the relative size of \( s_0 \) and \( s_1 \). If \( m_1 + m_2 < m_3 \), then \( s_0 = m_3^2 < s_1 \) (cf. case (i)), and the photon rate has its maximum at \( \omega = 0 \) and declines exponentially with power law corrections originating from \( \tilde{\sigma}(s) \) and other omitted factors in (4.1).

On the other hand, if \( m_1 + m_2 > m_3 \), then \( s_1 < s_0 \) (cf. case (ii)), and the rate has a maximum \( \propto e^{-(m_1 + m_2)/T} \) at \( \omega_p \). Furthermore, even for \( m_1 + m_2 > m_3 \), there will be a certain photon frequency \( \omega_s > \omega_p \) for which \( s_0 = s_1 \), implying that for \( \omega > \omega_s \) case (i) is applicable and the rate behaves as \( \propto \exp\{-\omega/T\} \) at large \( \omega \). Thus the mass ordering determines some basic features of the spectra, which is the reason why we have shown in the right panel of Fig. 3 the corresponding regions.

In Fig. 3, the photon spectra originating from four selected processes are plotted for three different positions in the phase diagram, corresponding to the chirally broken phase (a), the chirally restored phase (c) and the proximity of the CP (b). Comparing the spectra based on (3.1), one notices that in fact some of the processes develop a maximum at \( \approx \omega_p \) and vanish at \( \omega \to 0 \) while others seem to diverge in the IR limit as anticipated above by generalizing a previous consideration in [45]. With the above approximations one can understand why at different positions in the phase diagram the IR behavior of the photon rates is so different. It is the interplay of the masses of the involved modes and to a less extent the details of the interaction process. Since for the Compton process the sum of the incoming masses \( m_\psi + m_\pi,\sigma \) is larger than the mass of the outgoing quark \( m_\psi \), the corresponding contribution to the photon rate always has a maximum at finite photon energies. For the annihilation process there is a sensible dependence on the position in the phase diagram: In the
chirally broken phase, the sigma mass can be larger than twice the quark mass (cf. the diagonally hatched region in the right panel of Fig. 1). Therefore, there is no maximum of the rate at non-zero photon energy. Instead, the exponential factor approaches some finite value at $\omega = 0$ and other - in the former case subleading - effects get dominant. The most prominent effect stems from IR divergencies of the matrix elements which let the photon rate diverge as $\omega^{-2}$ at $\omega \to 0$ and thus needs to be regularized. In a band around the phase transition line and the pseudocritical region (horizontally hatched region in the right panel of Fig. 1) the meson masses are less than twice the quark mass (e.g. $m_\psi \sim m_\sigma \sim m_\pi \sim 200$ MeV at $(T, \mu) \sim (T_{CP}, \mu_{CP})$). Therefore, all processes lead separately to spectra which vanish at $\omega \to 0$ and have a maximum of similar height and an exponential tail at large $\omega$. From such a consideration one can already conclude that a divergency will not appear in a region of the phase diagram where the sigma mass is smaller than twice the quark mass. In the high temperature phase the quarks get light and the mesons heavy (cf. Fig 2).
Therefore, the annihilation rates have no maxima in the unhatched region of Fig. 1 (right panel) and hence are not exponentially suppressed at \( \omega \to 0 \) leading - together with the IR divergency of the matrix element - to a large photon rate at small \( \omega \). Thus the pattern of the rate behavior for the subprocesses shown in Fig. 3 can be explained quite naturally. Comparing parameter sets with different vacuum sigma masses, the above considerations imply a strong change of the low energy photon rates over the phase diagram if we contrast the emissivity of the L\( \sigma \)M with low vacuum sigma mass \( (m_{\sigma}^\text{vac} \lesssim 2m_{\psi}^\text{vac}) \) to the emissivity at higher vacuum sigma mass \( (m_{\sigma}^\text{vac} \gtrsim 2m_{\psi}^\text{vac}) \).

To highlight the role played by the matrix elements we also show in Fig. 4 the \( s \) dependence of \( \bar{\sigma} \). Again there are two types of functions: If \( m_1 + m_2 < m_3 \), \( \bar{\sigma}(s) \) diverges in the limit \( s \to s_0 \) like \( \sim (s - s_0)^{-1} \), and conversely, if \( m_1 + m_2 > m_3 \), then \( \bar{\sigma}(s) \) behaves like \( \sqrt{s - s_0} \). The reason for the divergence in the former case are IR divergencies of the matrix elements, because if \( s \gtrsim s_0 = m_{\psi}^2 \) the photon energy in the center of mass frame is small and thus the matrix elements are enhanced because the numerators in the propagators get small.
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5. Variation of photon rates over the phase diagram

The photon rates at fixed photon frequency depend sensitively on the position in the phase diagram as shown in [35] for $\omega = 10\text{MeV}$. A rate maximum in the critical region for the $\sigma$-involving Compton process was found. We focus here on higher values of $\omega$. From Fig. 5(d) one notices that up to $\omega \sim 50\text{MeV}$ the $\sigma$-involving Compton process (for which the available phase space around the critical point is enlarged, because of the small sigma mass) is the dominant channel and hence one can hope that a signal characteristic for the critical point can be obtained. For this frequency, the rates are depicted in Fig. 5. Several features are apparent. In the high temperature phase the Compton rates (a) and (c) are suppressed by many orders of magnitude relative to the corresponding annihilation processes (b) and (d). While the $\pi$-involving Compton rate is largest in the crossover region, the $\sigma$-involving Compton rate exhibits a global maximum in the critical region. In the low-temperature phase, the annihilation into a $\sigma$ meson and a photon is the strongest contributing process and shows the remnant of the structure seen in figure 2 in [35]. All of these observations can be explained with the above reasoning. The suppression of the Compton processes...
is explained by the different approximation schemes necessary for the two types of processes. Since $m_1 + m_2$ is for the Compton process always larger than $m_3 = m_1$, and $\omega = 50\text{MeV}$ is far below the peak frequency in the high temperature phase the exponential suppression factor $\exp\left\{-F(s_0)/T\right\}$ is many orders of magnitude smaller than the one for the annihilation case $\exp\left\{-(m_3 + \omega)/T\right\}$. For $\omega = \mathcal{O}(1 - 2\text{GeV})$ our results show no special features at $T_{pc}$ for small $\mu$.

6. Summary

Employing the linear sigma model (L$\sigma$M) we investigate whether the soft-photon emission rates can reflect the conjectured phase structure of QCD. The L$\sigma$M is chosen as a simple approach which exhibits a critical point (CP) at non-zero chemical potential. Relying on the L$\sigma$M field content, which is very schematic and mirrors only in a limited manner the proper degrees of freedom of QCD, we find, however, that the changes of the quasi-particle excitations masses within the phase diagram give rise to significant changes of the emission rates in selected channels. In particular, the spectral shapes depend strongly on the effective masses of excitation modes involved. This lets us hope that more advanced considerations can dig out peculiarities of the total emission rate, e.g. caused by the softening of the $\sigma$-type mode near the CP.

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