The Apollo Number: Space Suits, Self-Support, and the Walk-Run Transition

The MIT Faculty has made this article openly available. Please share how this access benefits you. Your story matters.

| Citation       | Carr CE, McGee J (2009) The Apollo Number: Space Suits, Self-Support, and the Walk-Run Transition. PLoS ONE 4(8): e6614. doi:10.1371/journal.pone.0006614 |
|----------------|---------------------------------------------------------------------------------------------------------------------------------------------|
| As Published   | http://dx.doi.org/10.1371/journal.pone.0006614                                                                                                                                                           |
| Version        | Final published version                                                                                                                                                                                     |
| Citable link   | http://hdl.handle.net/1721.1/52418                                                                                                                                                                       |
| Terms of Use   | Creative Commons Attribution                                                                                                                        |
| Detailed Terms | http://creativecommons.org/licenses/by/2.5/                                                                                                       |
The Apollo Number: Space Suits, Self-Support, and the Walk-Run Transition

Christopher E. Carr, Jeremy McGee
Massachusetts Institute of Technology, Cambridge, Massachusetts, United States of America

Abstract

**Background:** How space suits affect the preferred walk-run transition is an open question with relevance to human biomechanics and planetary extravehicular activity. Walking and running energetics differ; in reduced gravity (<0.5 g), running, unlike on Earth, uses less energy per distance than walking.

**Methodology/Principal Findings:** The walk-run transition (denoted *) correlates with the Froude Number (Fr=v²/gL, velocity v, gravitational acceleration g, leg length L). Human unsuited Fr* is relatively constant (~0.5) with gravity but increases substantially with decreasing gravity below ~0.4 g, rising to 0.9 in 1/6 g; space suits appear to lower Fr*. Because of pressure forces, space suits partially (1 g) or completely (lunar-g) support their own weight. We define the Apollo Number (Ap=Fr/M) as an expected invariant of locomotion under manipulations of M, the ratio of human-supported to total transported mass. We hypothesize that for lunar suited conditions Ap* but not Fr* will be near 0.9, because the Apollo Number captures the effect of space suit self-support. We used the Apollo Lunar Surface Journal and other sources to identify 38 gait events during lunar exploration for which we could determine gait type (walk/lope/run) and calculate Ap. We estimated the binary transition between walk/lope (0) and run (1), yielding Fr* (0.36±0.11, mean±95% C1) and Ap* (0.68±0.20).

**Conclusions/Significance:** The Apollo Number explains 60% of the difference between suited and unsuited Fr*, appears to capture in large part the effects of space suits on the walk-run transition, and provides several testable predictions for space suit locomotion and, of increasing relevance here on Earth, exoskeleton locomotion. The knowledge of how space suits affect gait transitions can be used to optimize space suits for use on the Moon and Mars.

Introduction

How space suits affect the walk-run transition is an open question with relevance to human biomechanics and extravehicular activity (EVA), a critical component of future human planetary exploration. Locomotion in space suits carries significant metabolic cost, which limits the intensity and duration, and hence value, of EVA. Walking and running incur different metabolic costs, and in reduced gravity environments (<0.5 g) running, unlike on Earth, uses less energy per unit distance than walking [1]. This finding also applies during space-suited locomotion [2,3]. Space suits adversely impact the metabolic cost of walking more severely than running, likely due to the spring-like nature of space suit pressure forces [3,4]. Space suits also appear to affect the walk-run transition; thus, space suits influence the energy cost of movement by influencing gait as well as by how they modify the metabolic cost of walking or running. Furthermore, by understanding how space suits impact the walk-run transition we can gain insight into the nature of gait transitions.

Here we develop a theory about how space suits may affect the walk-run transition based on a new non-dimensional parameter denoted the Apollo number, test the theory using data from the Apollo lunar surface missions of 1969–74, and explore the implications of our findings for EVA performance and discuss several testable predictions. First we summarize a simple model relating to the walk-run transition and show that our theory is a simple generalization of the concept of partial body-weight suspension (PBWS), a standard technique for simulating reduced gravity that is also used in rehabilitation. Then, we identify examples of walking and running gaits during lunar exploration and use them to test whether the Apollo number captures the effects of gravity and space suit self-support.

The Unsuited Walk-Run Transition

Humans appear to choose walking or running to minimize oxygen consumption at their current velocity [5]. The Froude number, a nondimensional quantity equal to the ratio of inertial to gravitational force, can be used empirically to predict the walk-run transition in bipeds and quadrupeds [5,6] according to the principle of dynamic similarity [6,7]. For a body in an environment with gravitational acceleration g, velocity v, and hip height or center of mass height L, the Froude number can be written as

Fr = v²/gL

The Froude number can be used to predict the preferred walk-run transition for any environment. However, the Froude number does not account for the effects of space suits on the walk-run transition. We hypothesize that a new non-dimensional parameter, the Apollo Number (Ap), will capture the effects of space suit self-support. The Apollo Number is defined as

Ap = Fr/M

where M is the ratio of human-supported to total transported mass. The Apollo Number is expected to be an invariant of locomotion under manipulations of M, and will be near 0.9 for lunar suited conditions. We used the Apollo Lunar Surface Journal and other sources to identify 38 gait events during lunar exploration for which we could determine gait type (walk/lope/run) and calculate Ap. We estimated the binary transition between walk/lope (0) and run (1), yielding Fr* (0.36±0.11, mean±95% CI) and Ap* (0.68±0.20).

Conclusions/Significance:

The Apollo Number explains 60% of the difference between suited and unsuited Fr*, appears to capture in large part the effects of space suits on the walk-run transition, and provides several testable predictions for space suit locomotion and, of increasing relevance here on Earth, exoskeleton locomotion. The knowledge of how space suits affect gait transitions can be used to optimize space suits for use on the Moon and Mars.
Modeling walking as an inverted pendulum [8] yields the constraint that walking can only occur for $Fr < 1$ (Text S1).

The walk-run transition, which we denote by $\ast$, has generally been observed to occur in humans near $Fr \approx 0.5$ [6], consistent with the maximum walking speed constraint of the idealized inverted pendulum model. While the model does not predict a particular value for $Fr$, dynamic similarity [7] predicts constant $Fr$ despite changes in $g$ and $L$, all other factors being equal, and this prediction is independent of any particular model of walking [9].

To understand how gravity effects $Fr$ and to gain insight into locomotion energetics, studies have used partial body-weight suspension (PBWS) to simulate reduced gravity by applying a relatively constant upward force on the center of mass using a harness [1,10,11,12]. These studies report Froude numbers based on the effective gravity level $g_{eff}$, so that $Fr_{eff} = \frac{v^2}{(g_{eff} L)}$. Here, $g_{eff} = Mg$, where $g$ is the actual gravitational acceleration and $M$ is the ratio of human supported to total transported mass (supplemental materials).

Kram et al. [11] found unsuited $Fr_{eff}$ changed little from simulated reduced gravity levels down to 0.4 g, consistent with dynamic similarity, but increased to 1.1 as $g_{eff}$ decreased further to 0.1 g; Kram et al. [11] did not measure $Fr_{eff}$ at lunar gravity (~1/6 g), but interpolation yields $Fr_{eff} = 0.9$. Kram et al. [11] attributed part of the increase in $Fr_{eff}$ below 0.4 g to imperfection in the simulation method, but measurements of $Fr$ in true reduced gravity conditions during parabolic flight on board NASA's C-9 aircraft suggest that PBWS may be more accurate than previously assumed [13].

Substantially reduced gravity, then, appears to elevate $Fr$, although $Fr$ matches predictions of dynamic similarity over a greater than two-fold change in $g$. Space suits, in contrast, appear to decrease $Fr$, although controlled experiments involving running in space suits are rare, in part because 1 g space-suited running requires metabolic rates above the lactate threshold [2].

### Space Suit Self-Support

Just as PBWS affects the ratio of human carried to total transported mass $M$, so does a space suit: internal pressure forces may support part or all of the space suit weight (supplemental materials). Rewriting $Fr_{eff}$ in terms of a Froude number involving the true gravitational acceleration and the mass ratio $M$ gives us a new quantity that we define as the “Apollo number” or $Ap$ (Text S1):

$$ Ap = \frac{Fr}{M} = \frac{v^2}{gL} = \frac{1}{M} = \frac{v^2}{gML} = Fr_{eff}, $$

with the same idealized restriction for walking of $Ap \leq 1$.

In the case of no space suit, $M=1$ and $Ap=Fr$. If the only space suit-related factor affecting the walk-run transition is $M$, the fraction of total mass carried by the human, then the Apollo Number at the walk-run transition should be equal in value whether suited or unsuited. In this situation, the walk-run transition depends directly on the ratio of inertial to net gravitational force. This hypothesis is identical to the proposition that $Fr_{eff}$ is constant across simulated gravity levels (supplemental materials), which appears to be a good approximation for $M \geq 0.4$ [11].

Therefore, for space-suited lunar locomotion, we hypothesize that $Ap$ will be closer to the unsuited $Fr$ (~0.9) than with $Fr$, because the Apollo Number captures the effect of space suit self-support. Stated in an alternative manner, dynamic similarity predicts that space suits will reduce $Fr$ by about $1/M$ relative to unsuited $Fr$.

### Methods

The Froude and Apollo numbers depend upon physical characteristics including leg length and body mass, so we assembled these data for the astronauts who explored the lunar surface (Table 1).

We exhaustively reviewed audio transcripts and video clips of lunar EVAs available from the Apollo Lunar Surface Journal [14], and several NASA technical reports related to lunar surface locomotion [15,16,17] to identify gait events on the lunar surface for which we had some evidence of the gait type (walk/lope/run) and could estimate locomotion velocity (see below). Using the locomotion velocities and subject characteristics we estimated $Fr$ for each event.

We took total transported mass as the sum of body mass and estimated suit mass at the time of each event. We approximated the space suit mass based on the suit type (A7L, used for Apollo 11–14, or the A7LB, the latter used for the Apollo 15–17 missions) and by assuming a constant consumables usage rate during each EVA (Table 2), an accurate approximation based on subsequent analysis of metabolic rates (Figure 1). Space suit self-support, modeled as an idealized pressurized column, is limited by the minimum cross section, found at the ankle joint (Figure 2). We assumed complete space suit self-support based on calculations using space suit ankle joint measurements (Nicole Jordan, personal communication) and video data of lunar astronauts (Text S1, Video S1). After estimating $M$, we computed $Ap$ for each gait event.

On Earth, humans commonly use only walking and running gait, but on the Moon, astronauts used a variety of hopping-like gaits often referred to in prior studies as loping. Loping, often like

| Table 1. Apollo Lunar Surface Astronaut Characteristics. |
| --- |
| **ID** | **Mission** | **Role** | **Last Name** | **Mass** | **Height** | **Li** |
| 1 | 11 | CDR | Armstrong | 76.2 | 1.80 | 0.97 |
| 2 | 11 | LMP | Aldrin | 75.5 | 1.78 | 0.96 |
| 3 | 12 | CDR | Conrad | 66.8 | 1.69 | 0.91 |
| 4 | 12 | LMP | Bean | 66.3 | 1.77 | 0.95 |
| 5 | 14 | CDR | Shepard | 76.4 | 1.80 | 0.97 |
| 6 | 14 | LMP | Mitchell | 80.1 | 1.80 | 0.97 |
| 7 | 15 | CDR | Scott | 79.6 | 1.83 | 0.99 |
| 8 | 15 | LMP | Irwin | 72.0 | 1.73 | 0.93 |
| 9 | 16 | CDR | Young | 77.2 | 1.75 | 0.95 |
| 10 | 16 | LMP | Duke | 71.8 | 1.82 | 0.98 |
| 11 | 17 | CDR | Cernan | 78.2 | 1.83 | 0.99 |
| 12 | 17 | LMP | Schmidt | 73.9 | 1.75 | 0.95 |

Roles: Commander (CDR) and Lunar Module Pilot (LMP).

1Body mass estimated as mean of F-0 (Flight Day) and R+D (Return Day) masses in Table 16 of Biomedical Results of Apollo [25].

1Height from astronaut biographies in the Apollo 11–17 Press Kits, available from the Apollo Lunar Surface Journal [14].

1Leg length $L$ estimated as Height/1.85, following [2].

doi:10.1371/journal.pone.0006614.t001

Role: Commander (CDR) and Lunar Module Pilot (LMP).
skipping but without the support-foot exchange [18], shares features of walking and running [18,19].

To analyze astronaut gait in terms of a binary transition, we assigned a binary variable \( gait \) (walk or lope = 0, run = 1) for each event. We analyzed the variable \( gait \) using a standard logit model (methods) to estimate the transition probability \( P \) (probability that \( gait = 1 \)) for both \( Fr \) and \( Ap \) and determine the estimated walk-run transition, or point where \( P \approx 1/2 \).

Finally, to facilitate comparisons at lunar gravity, we fit unsuited \( Fr/\text{C}^3 \) eff values from Kram et al. [11] using the power law \( Fr/\text{C}^3 \) eff = \( C(G)^k \), and found \( C = 0.42 \pm 0.06 \) (mean \( \pm 95\% \text{CI} \)), with an adjusted \( R^2 = 0.98 \).

Gait Type and Velocity Estimation During Lunar EVA

Allowable evidence for the gait type included specific mention of gait type in the audio transcripts or associated written commentary in [14], observation of gait type via video clip, or written description of the gait type in the case of the NASA technical reports [15,16,17], which were written specifically to analyze human movement on the lunar surface.

Velocities derived from the Apollo Lunar Surface Journal [14] and the NASA technical reports [15,16,17] are based on extensive reconstructions of astronaut time and distance measurements, the latter frequently determined from calibrated images of the lunar surface. We did not extract time and position data from videos but relied upon prior measurements of known time and position. For example, gait condition 10 (Table S1) is based on video determination of gait type and velocity determination from commentary in [14] that reads: “Neil’s run across the TV picture takes about 25 seconds. According to Figure 3–16 in the Apollo 11 Preliminary Science Report, the distance he covered in this time is 22 meters. His running speed is, therefore, about 3.2 km/h [0.89 m/s].”

All of the videos analyzed and the source for video S1 are in the public domain and are not copyrighted (image credits: NASA/Ken Glover).

Space Suits are Self-Supporting in Lunar Gravity

Imagine an inflatable column, torque stabilized so that it cannot buckle prematurely; the maximum mass supported by this
stabilized column, an idealized approximation of a space suit leg, is given by \( m_S = pA/g \), where \( p \) is the differential pressure across the column wall, \( A \) is the minimum cross section, and \( g \) is the gravitational acceleration acting on the mass.

For a space suit in a vacuum (Figure 2), \( p \) is the internal suit pressure, and \( A \) is the cross-sectional area of the ankle joint (the point of minimum cross-sectional area), so that the force supported by a single space suit leg is \( F_S = pA - T \), where \( T \) is the tension in the load-bearing “skin” of the space suit, known as the restraint layer, at the cross section. For high suit weights (e.g. on Earth) or low pressures \( p \), the maximum net force \( F_S \) occurs when \( T = 0 \) so that \( F_S = pA = m_S g \), and the self-support is partial \((m_{body}/m - M \leq 1, \text{where } m_{body} \text{ is the mass of the astronaut, and } m \text{ is the total transported mass}) \). Because the maximum net force \( F_S \) cannot exceed the suit weight, at low suit weights (e.g. on the Moon) or high pressures, the maximum net force is equal to the suit weight and self-support is complete \((M = m_{body}/m)\).

Consider the pressure forces transmitted by a single space suit leg with a minimum cross section diameter of 14.6 cm or 5.75 inches. This value represents the approximate ankle ring inner diameter of the current NASA EMU space suit and the approximate diameter of the most narrow ankle cross section of the Apollo A7LB suit, which had no ankle ring (unpublished observations, Nicole Jordan). For a suit pressure of 26.2 kPa (3.8 psi) and minimum cross sectional area of 168 cm² \((26.0 \text{ in}^2)\), the pressure force of \( pA = 439N \) exceeds the 156N lunar weight of the A7LB at its maximum mass condition \((96 \text{ kg})\) by a factor of 2.8. Thus, a space suit on the lunar surface can be considered entirely self-supporting at the walk-run transition, where the time-averaged number of legs in contact with the ground is approximately one.

Direct evidence of this assertion is provided by videos of the Apollo astronauts demonstrating the challenge of reaching the lunar surface: the high pressure forces \((pA > F_S) \) so that \( T > 0 \) made it challenging to fully buckle the knee joint, even when standing on one leg. In one case (Apollo 16, 146:49:41, Video S1) an astronaut can be seen jumping into the air in an attempt to provide (during the following impact) enough force (through body weight and impact loads) to buckle the knee joint and reach a hammer on the lunar surface.

**Logit Transition Model**

Generalized linear models (GLMs) relate the random distribution of a measured variable to a linear predictor through a link function, the appropriate choice of which depends upon the distribution of the measured variable. In our case, the measured variable is \( gait \) \((\text{walk}/\text{lope} = 0, \text{run} = 1)\), and the predictor variable \( x \) is \( Fr \) or \( Ap \). Because gait is binomial, the proper canonical link function is the logit. For probability \( P \), the odds ratio is given by \( P/(1-P) \), and the logit transformation defined as \( \text{logit}(P) = \log[P/(1-P)] \). Here, \( P(x) \) is the probability that \( gait = 1 \), and can be expressed as

\[
P(x) = \frac{1}{1 + \exp[-(\alpha + \beta x)]}
\]

which has the convenient property that \( \text{logit}(P) = \alpha + \beta x \), making this widely applicable model also easy to fit. The two parameters \( \alpha \) and \( \beta \) describe the shape and location of the state transition, with the transition point \( x = -\alpha/\beta \) defined by \( P(x) = 0.5 \).

The data were fit using the MATLAB GLM fitting function glmfit() (The Mathworks, Natick, MA), which calculates the parameters \( \alpha \) and \( \beta \), the variance estimates \( \sigma^2_\alpha \) and \( \sigma^2_\beta \), and the covariance \( \text{cov}(\alpha, \beta) \). The standard error of the transition point was estimated as

\[
\delta_{LDSS} = \sqrt{\frac{\sigma^2_\alpha + \sigma^2_\beta - 2 \text{cov}(\alpha, \beta)}{N}}
\]

**Results and Discussion**

We identified and analyzed 38 classifiable gait events (Figure 3, Table S1) with mean \( M = 0.49 \). Of these events, 10 involved walking, 10 loping, and 18 running. Walking and loping generally occurred at lower Froude or Apollo numbers than running; there was no significant difference between the mean \( Fr \) for walking and loping (two-tailed t-test, \( p = 0.95 \)). We pooled walking and loping data on the basis of two considerations: First, loping Froude numbers are statistically indeterminate from those of walking. Second, walking and loping share the exchange of kinetic and potential energy of the center of mass that is absent in running.

All logit parameters for fits to \( Fr \) and \( Ap \) data (Figure 4) were significant (Table 3), and the walk-run transitions for \( Fr \) \((0.36 \pm 0.11, \text{mean } \pm 95\% \text{ CI}) \) and \( Ap \) \((0.68 \pm 0.20) \) were significantly different \((p < 0.001)\). Our estimated lunar suited \( Fr^* \) and \( Ap^* \) values were 60% and 24% lower, respectively, than the estimated lunar unsuited \( Fr_{eff}^* = 0.90 \) from the Kram et al. [11] power law fit (Figure 5, gray line; \( G = g/g_{\text{earth}} \)).

As a rough test of our hypothesis, we conclude that the Apollo number is closer to the unsuited Froude number \((~0.9)\) than the (suited) Froude number. Similarly, the \( Fr_{eff}^*/Fr_{suited}^* \) ratio of 2.51 differs from the expected value of \( 1/M = 2.04 \) by 23%.

Kram et al. [11] adjusted \( Fr_{eff}^* \) to account for the downward inertial force caused by the swing leg (which experienced 1 g forces that would not be present in true reduced gravitational environments), causing their adjusted \( Fr_{eff}^* \) values to range from 0.39 in 1 g to 0.67 in 0.1 g. However, experiments in NASA’s C-9 aircraft, which produces the closest Earth-analog to lunar gravity by flying modified parabolic flight profiles, have measured unsuited \( Fr^* = 1.39 \pm 0.45 \) (mean \( \pm \text{s.d.}, N = 6 \) [13]). Thus, the aforementioned adjustment may represent a substantial overcorrection. G-level fluctuations during parabolic flight, and the short period \((~30 \text{ s})\) of lunar gravity available per trial may contribute to the high measured \( Fr^* \); for example, slightly lower g-levels could produce higher \( Fr^* \) estimates because the \( Fr_{eff}^* \) vs.
gravity curve is quite steep near 1/6 g (Figure 5). However, an experiment on NASA’s POGO [13], a high-fidelity (2–10% dynamic error) pneumatic controlled partial body-weight suspension device [20], found unsuited Fr/C₃ ≈ 1.22 ± 0.26 (mean ± s.d., N = 4).

Taking the unadjusted Kram et al. [11] data as representative of true unsuited Fr*, the Apollo Number explains 60% of the difference between the lunar suited Fr/C₃ (0.36) and lunar unsuited Fr*. If NASA POGO estimates (Fr/C₃eff, 1.22) are more representative, then the Apollo Number explains 38% of this difference. Thus, changes in the walk-run transition speed in suited versus unsuited locomotion appear attributable, at least in part, to space suit self-support.

Inherent limits to the dataset restrict the fidelity of our analysis: For example, conditions 1–9 (Table S1) are derived from a single three-minute period during astronaut Aldrin’s gait and mobility evaluation (a prime objective of Apollo 11), and may admit the highest risk of subject bias of any set of gait events in Table 2. Fitting a restricted dataset, without conditions 1–9, results in Fr/C₃ = 0.478 ± 0.158 (mean ± 95%CI) and Ap/C₃ = 0.876 ± 0.314, suggesting that the Apollo Number may explain more of the observed difference in the suited versus unsuited locomotion appear attributable, at least in part, to space suit self-support.

Unsurprisingly, the Apollo Number does not completely explain the observed difference: space suits may impact the walk-run transition speed through factors other than self-support, and our assumption of perfect self-support is itself an approximation. It is unknown whether gait transitions are triggered via metabolic signals [5], by muscle force production or activation [21], or by other factors such as stability [22]. Space suits may also influence the walk-run transition through mobility restriction, increased joint mechanical work due to joint torques (generated in large part from pressure-volume work resulting from non-constant volume joints), changes in mass distribution and thus stability, and other as
yet unquantified factors such as leg stiffness changes that may modify gait dynamics. Finally, although all gait conditions had \( M > 0.4 \), the gravity dependence of \( Fr_{off} \) suggests that for \( M < 0.1 \) the Apollo number may not fully capture the effect of space suit self-support (supplemental materials).

Despite these limitations, our theory of invariant \( Ap^* \) despite manipulations of loading (\( M \)) provides several testable predictions. First, at higher suit masses with continued full self-support (\( M \)), the walk-run transition will occur at a lower speed (\( Fr \)). Because running in a space suit has a lower cost of transport (energy/distance) than walking [23, 3], lowering the walk-run transition may provide energetic benefits that permit expansion of the region able to be explored during an EVA. In an idealized model, the “walkback” restriction allows exploration of the region defined by a circle with a radius, determined by remaining consumables (oxygen, CO2 scrubbing capability, cooling water), that shrinks with time. Space-suited running may have low cost of transport, but absolute metabolic rates are still high (for example, 326W and 429W for two running conditions during Apollo 16 [16]). Under conditions of full self-support, large suit mass may reduce the walk-run transition speed, facilitating efficient locomotion at lower and more sustainable metabolic rates.

Second, when carriage of large loads reduces self-support (\( \uparrow M \)), walking becomes possible at higher velocities (\( \uparrow Fr \)). The only walking condition involving a heavy load (Table S1, condition 36) occurred during transport of the 116 kg Apollo Lunar Surface Experiments Package via carry-bar to its deployment site. For this \( (Fr = 0.52, Ap = 0.77) \) condition, \( P(Fr) = 0.78 \) and \( P(Ap) = 0.59 \) (restricted dataset: \( P(Fr) = 0.61, P(Ap) = 0.34 \)). This is consistent with a near constant \( Ap^* \), where the condition represents a gait near (technically slightly above) the run transition walk; this condition is completely concordant with the higher \( Ap^* \) of the restricted dataset, where it would be expected to represent a walk. However, the condition is above \( Fr^* \) and the condition’s \( Fr = 0.52 \) is significantly elevated (one-sided z-test, \( z = 5.52, p < 0.001 \)) relative to all other walking conditions, none of which included similar loads. The data support the theoretical increase in \( Fr^* \) with increased human-supported load fraction (\( \uparrow M \)).

A third prediction relates to changes in the walk-run transition when humans use exoskeletons with external load paths, such as those under consideration for load-carrying [23] or those used for medical rehabilitation [24]. Consider a human wearing an exoskeleton that supports an additional body weight equivalent of mass, so that \( M = 0.5 \). For an unsuited \( Fr^* \sim 0.3 \), we might expect (taking \( L = 0.95 \) m) a walk-run transition velocity near \( v^* \sim 2.2 \) m/s (4.8 mph). With the exoskeleton (\( M = 0.5 \)) we might now expect \( Ap^* \sim 0.5 \), \( Fr^* \sim 0.25 \), and \( v^* \sim 1.5 \) m/s (3.4 mph), a rather slow and potentially energetically inefficient running velocity in 1 g. Experimental verification that external load paths modify \( Fr^* \) in the expected manner has been demonstrated using a lower-body exoskeleton designed to simulate the knee joint-torques of the current NASA spacesuit (C. Carr, unpublished observations). Knowing the walk-run transition and its energetic consequences during exoskeleton locomotion could be useful in determining the range of transport speeds consistent with efficient exoskeleton usage, and may guide the design of exoskeletons, such as inclusion of high energy-return springs optimized for a particular speed, frequency, or range of motion.

In summary, we have developed a theory of how \( M \), the ratio of human supported to total transported mass, affects the walk-run transition and tested this theory using gait events from space-suited lunar locomotion. The Apollo Number \( (Ap = Fr/M) \) appears to explain a significant part of the difference between the unsuited and suited walk-run transition Froude numbers, and as expected, space-suited \( Fr^* \) is well below the unsuited \( Fr^* \). Several predictions can now be tested: if our theory is correct, manipulation of self-support, whether by changes in space suit pressure or mass, gravitational environment, or via exoskeleton load carrying, will change the walk-run transition speed but have little effect on the Apollo Number. Indeed, PBWS experiments have shown that humans have near constant \( Ap^* \) for moderate reductions in simulated gravity, and that exoskeletons with external load paths lower the walk-run transition speed.

Supporting Information

Text S1
Found at: doi:10.1371/journal.pone.0006614.s001 (0.22 MB DOC)

Table S1 Classifiable Gait Events During Lunar Locomotion
Found at: doi:10.1371/journal.pone.0006614.s002 (0.16 MB DOC)

Video S1 Apollo space suits self-support in lunar gravity. During this scene from Apollo 16, Astronaut Charles Duke drops a hammer on the lunar surface, then jumps repeatedly in order to overcome the self-support of the space suit by compressing the space suit knee joint(s) so that he might retrieve the hammer from the surface.

Found at: doi:10.1371/journal.pone.0006614.s003 (4.85 MB MOV)

Acknowledgments

We thank Nicole Jordan for space suit measurements.

Author Contributions

Conceived and designed the experiments: CEC. Analyzed the data: CEC JM. Contributed reagents/materials/analysis tools: CEC. Wrote the paper: CEC JM.

References

1. Farley CT, McMahon TA (1992) Energetics of walking and running: insights from simulated reduced-gravity experiments. Journal of Applied Physiology 73: 2709–2712.
2. Carr CE, Newman DJ (2005) When is running more efficient than walking in a space suit? SAE Transactions Journal of Aerospace 114: July 2005 (paper No. 2005-2001-2970).
3. Carr CE, Newman D (2007) Space suit bioenergetics: Framework and analysis of Classifiable Gait Events During Lunar Locomotion Table S1.
4. Carr C, Newman D (2005) When is running more efficient than walking in a space suit? SAE Transactions Journal of Aerospace 114: July 2005 (paper No. 2005-2001-2970).
5. Alexander RM (2001) Walking on other planets. Nature 409: 467 p, 469 p.
6. Minetti AE (2001) Walking on other planets. Nature 409: 467 p, 469 p.
7. Bullimore SR, Donelan JM (2007) Criteria for dynamic similarity in bouncing gait. Journal of Theoretical Biology doi:10.1016/j.jtbi.2007.09.031.
8. Medow S, McMahon TA (1989) Ballistic walking: an improved model. Mathematical Biosciences 52: 241–260.
9. Alexander RM (1996) Walking and Running. The Mathematical Gazette 80: 262–266.
10. Griffin TM, Tolani NA, Kram R (1999) Walking in simulated reduced gravity: mechanical energy fluctuations and exchange. Journal of Applied Physiology 86: 383–390.
11. Kram R, Domingo A, Ferris DP (1997) Effect of reduced gravity on the preferred walk-run transition speed. Journal of Experimental Biology 200: 821–826.
12. Grabinowski A, Farley CT, Kram R (2005) Independent metabolic costs of supporting body weight and accelerating body mass during walking. Journal of Applied Physiology 98: 579–583.
13. Hagan D, DeWitt J, Bentley J (2006) Evaluation of the effectiveness of overhead suspension reduced-gravity analogs in a microgravity environment. In: Skinner NC, ed. C-9 and Other Microgravity Simulations, Summary Report (NASA Report No TM-2006-213727). Houston, Texas: National Aeronautics and Space Administration, Lyndon B. Johnson Space Center. pp 161–171.

14. Jones E (2006) Apollo Lunar Surface Journal. NASA History Website.

15. Kubis J, Elrod J, Rusnak R, Barnes J (1972) Apollo 15 time and motion study. National Aeronautics and Space Administration.

16. Kubis J, Elrod J, Rusnak R, Barnes J, Saxon S (1972) Apollo 16 time and motion study. National Aeronautics and Space Administration.

17. Kubis J, Elrod J, Rusnak R, McLaughlin E, Moseley E (1970) Apollo XI lunar EVA (Mobility Evaluation). In: Manned Spacecraft Center H, Texas, editor: National Aeronautics and Space Administration.

18. Rader A, Newman D, Carr C. Loping: a strategy for reduced gravity human locomotion? 2007 July 9–12, 2007; Chicago, Illinois. SAE paper 2007-01-3134. Society of Automotive Engineers, Inc., Warrendale, Pennsylvania, USA.

19. Minetti AE (1998) The biomechanics of skipping gaits: a third locomotion paradigm? Proceedings Biological sciences/The Royal Society 265: 1227–1235.

20. Ray D (1994) Partial gravity simulation using a pneumatic actuator with closed loop mechanical amplification. NASA Johnson Space Center.

21. Neptune RR, Sasaki K (2005) Ankle plantar flexor force production is an important determinant of the preferred walk-to-run transition speed. Journal of Experimental Biology 208: 799–808.

22. Diedrich FJ, Warren WH Jr (1995) Why change gaits? Dynamics of the walk-run transition. Journal of experimental psychology Human perception and performance 21: 183–202.

23. Walsh CJ, Endo K, Herr H (2007) A quasi-passive leg exoskeleton for load-carrying augmentation. International Journal of Humanoid Robotics: (In press).

24. Hesse S, Schmidt H, Werner C, Bardeleben A (2003) Upper and lower extremity robotic devices for rehabilitation and for studying motor control. Current opinion in neurology 16: 703–710.

25. Johnston R, Dietlein L, Berry C (1975) Biomedical Results of Apollo: National Aeronautics and Space Administration.