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A Double Helix Flux Pipe-Based Inductive Link for Wireless Charging of Electric Vehicles

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Abstract: This paper presents a novel inductive link for wireless power transfer (WPT) system of electric vehicles (EVs). The WPT technology uses an alternating magnetic field to transfer electric power through space. The use of the WPT technology for charging electric vehicle provides an excellent alternative to the existing plug-in charging technology. It has been reported that the inductive link using planar coils such as the circular and rectangular coil are capable of transferring a high power with high efficiency. However, they have a poor tolerance for lateral misalignment, thus their power transfer efficiency decreases significantly with the misalignment. Due to the poor misalignment performance of the planar coil topology, extensive studies have been carried out on the flux pipe topology due to their excellent misalignment tolerance. To address this, in this paper, a novel inductive link using double helix flux pipe topology is proposed. The performances of the inductive link using the proposed double helix flux pipe are analyzed and compared with inductive links using conventional flux pipe. The proposed model has excellent characteristics in terms of the power transfer efficiency and tolerance against misalignments. The proposed model is capable of transferring over 1.6 kW of power with a coil-to-coil efficiency of over 98.5% at a load resistance of 20 Ω.

Keywords: double helix flux pipe; electric vehicle; inductive link; misalignment tolerance; wireless power transfer

1. Introduction

Wireless charging technology is attracting attention for charging the batteries of electric vehicles (EVs). Inductive power transfer (IPT) is one of the most commonly used technologies to perform wireless charging [1–10]. A typical IPT system is composed of a transmitter coil and receiver coil which enables electric power transfer by alternating magnetic field. The current is passed through the transmitter coil which produces an alternating magnetic field, thus inducing a current in the receiver coil which can be used to charge the battery of EV. The technologies use a friendlier and convenient charging process. They offer the advantage of eliminating the hazards, especially when using an old and cracked cable, which expose the user to an electrical shock.

The performance of the IPT system depends on the structure and characteristics of the compensation network, converter and coil. In particular, the inductive link, including two coils, has a significant impact on the performance of IPT systems. The performances of the inductive link depend on the coil configuration design, coil alignment, material property of ferromagnetic core, and configuration of the ferromagnetic core. A practical inductive link design involves the selection of an appropriate ferromagnetic core and configuration of two coils [11]. It was noted that coil geometry significantly impacts the power transfer efficiency. Planar coils, such as flat circular coils, rectangular coils, and bipolar coils, are capable of transferring electrical power with high efficiency. However, the limitation of the
planar coil includes high sensitivity to misalignment between two coils, which leads to inefficient power transfer \([11–13]\). The misalignment is inevitable due to limited parking accuracy. In addition, to reduce charging times, it is necessary to perform IPT at a reasonable power level, which requires high magnetic coupling.

This paper proposes a novel inductive link, which use double helix (DH) flux pipe structure. In this flux pipe, two helical coils are tilted at opposite angles of 45° to form a cross configuration. The proposed DH flux pipe magnifies the coupling coefficient and high misalignment tolerance. Here, the coupling coefficient is the ratio of the mutual impedance to the square root of the product of the self-impedances of the coupled circuits. The coupling coefficient is an important parameter for inductive links, and it is related to how much power from the generated electromagnetic (EM) field is induced in the secondary coil. The coupling coefficient and power transfer efficiency of inductive link applying the DH flux pipe is analyzed based on the finite element analysis. The proposed configuration can be utilized as an efficient inductive link for existing IPT system of the EV which has the large misalignment and thus the low power transfer efficiency.

2. Double Helix Flux Pipe-Based Inductive Link

2.1. IPT System Using SS Topology

The basic block diagram of the IPT system for EVs is illustrated in Figure 1. To enable power transfer from the transmitter coil to the receiver coil, AC power from the grid is converted into high frequency (HF) AC power AC/DC and DC/AC converters. In the IPT system, a compensation network is necessary to reduce the leakage inductance because the primary coil (TX coil) and the secondary coil (RX coil) are loosely coupled. The compensation capacitors are generally used for compensating the leakage inductance. The compensation networks can be classified into four types: the series-series (SS), parallel-parallel (PP), series-parallel (SP), and parallel-series (PS) types. Source compensation is used to reduce the reactive power on the transmitter side \([11,14]\), and receiver compensation is used to maximize the power transfer and efficiency. The features of the compensation networks are listed in Table 1 \([15,16]\). From Table 1, we can see that the primary capacitance of the SS topology has a constant value, regardless of the coupling coefficient and load conditions. On the other hand, the capacitances in SP topology vary when the coupling coefficient changes. For PS and PP topology, the capacitances depend on both the coupling coefficient and load conditions. The type of compensation network can be selected using the specific application requirements for the IPT system \([17–21]\). The series-series (SS) compensation topology is suitable for charging EV battery because the capacitance on the primary side is independent of the load and magnetic coupling coefficient \([22,23]\).

![Figure 1. Block diagram of general inductive power transfer (IPT) system.](image-url)
Table 1. Features of compensation networks.

| Type      | Primary Capacitance, $C_p$ | Secondary Capacitance, $C_s$ | Load Resistance, $R_L$ |
|-----------|----------------------------|------------------------------|------------------------|
| SS topology | $\frac{C_p L_S}{L_T}$     | $\frac{1}{\omega_0^2 L_R}$  | $\frac{\omega_0 L_S}{Q_R}$ |
| PP topology | $\frac{C_p L_S}{L_T}$     | $\frac{1}{\omega_0^2 L_R}$  | $\frac{\omega_0 L_S}{Q_R}$ |
| SP topology | $\frac{C_p L_S}{L_T}$     | $\frac{1}{\omega_0^2 L_R}$  | $\frac{\omega_0 L_S}{Q_R}$ |
| PS topology | $\frac{C_p L_S}{L_T}$     | $\frac{1}{\omega_0^2 L_R}$  | $\frac{\omega_0 L_S}{Q_R}$ |

The equivalent circuit model of the IPT system applying SS compensation topology is shown in Figure 2. In this IPT system, load resistance can be calculated as follows:

$$R_L = \frac{\omega_0 L_S}{Q_S} \tag{1}$$

where $Q_S = \omega_0 L_S/R_S$. When the inductances of $T_X$ coil and $R_X$ coil are $L_P$ and $L_S$, respectively, the compensation capacitance at the primary side and secondary side can be expressed as follows:

$$C_p = \frac{1}{(\omega_0^2 \times L_P)}, \quad C_s = \frac{1}{(\omega_0^2 \times L_S)} \tag{2}$$

Figure 2. The IPT system model using series-series (SS) compensation topology.

Also, the total impedance $Z_T$ of the inductive link is calculated by Equation (3).

$$Z_T = R_P + (\omega_0^2 \times M^2)/(R_S + R_L) \tag{3}$$

where $R_P$, $R_S$, and $M$ are the $T_X$ coil resistance, $R_X$ coil resistance, and mutual inductance between the two coils, respectively. In addition, the quality factors of the $T_X$ coil $Q_P$ and $R_X$ coil $Q_S$ can be expressed as follows:

$$Q_T = \omega_0 L_P/R_T, \quad Q_S = \omega_0 L_S/R_S \tag{4}$$

For IPT systems, the coupling coefficient $k$ is very small because the two coils are coupled very loosely. For the series-series (SS) topology, the $T_X$ coil and $R_X$ coil are connected to the compensation capacitors in series. When the capacitors are added to the primary side and secondary side, the system resonates, and the power transferred to the load increases. If the currents through the $T_X$ coil and the $R_X$ coil are $I_P$ and $I_S$, respectively, the output power is written as follows:

$$P_{out} = I_P^2 R_L = (\omega_0 M I_P/(R_P + R_S))^2 R_L = \left(\omega_0 k I_P \sqrt{L_P L_S}/(R_P + R_S)\right)^2 R_L \tag{5}$$

In addition, the input power can be expressed as follows:

$$P_{in} = I_P^2 R_P + I_S^2 (R_S + R_L) \tag{6}$$
The transfer power efficiency can be calculated by Equation (7).

$$\eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{R_L}{\left( (R_S + R_L)^2 / (k^2 Q_P Q_S R_S) + R_S + R_L \right)}$$

(7)

The maximum efficiency is achieved at $R_P/R_S = (1+k^2 Q_P Q_S)^{1/2}$, and it can be expressed as follows:

$$\eta_{\text{max}} = \frac{k^2 Q_P Q_S}{\left( 1 + \sqrt{1 + k^2 Q_P Q_S} \right)^2}$$

(8)

According to Equation (7), the transfer power efficiency depends on the coupling coefficient between the $T_X$ coil and the $R_X$ coil, and the larger the coupling coefficient, the higher the efficiency.

2.2. Flux Pipe for IPT System

Magnetic couplers can be classified into planar type and solenoid type. The planar type has a magnetic field structure to perpendicularly pass from its center, and it is very sensitive to misalignment [24,25]. In particular, the coupling coefficient of the planar type becomes nearly zero when the lateral misalignment is approximately 40% of the coil size. The solenoid type has a magnetic field structure parallel to the coils, so it is less sensitive to misalignment [26–29]. For the solenoid type, if the secondary coil is moved laterally from the center of the primary coil, the total flux penetrating the secondary winding will decrease only slightly, and the reduction in the coupling coefficient will be small. Therefore, the solenoid type has excellent tolerance to lateral misalignment. Figure 3 shows magnetic field structures according to different winding types.

Figure 4 shows configurations and dimensional parameters of the $R_X$ coils for flux pipe-based inductive link. The ideal solenoid coil for the flux pipe can be used to simplify modeling, but it is not an accurate model because it requires a turn-to-turn pitch when the solenoid coil is actually manufactured. The helix model, on the other hand, is relatively accurate compared to the ideal solenoid because it takes into account the turn-to-turn pitch that can occur during production. In this paper, we set the helix angle of the coil to 45° and all other specifications such as the winding turns and coil sizes.

![Figure 3. Magnetic field by magnetic coupler type: (a) planar type and (b) solenoid type.](image_url)
The double helix coil is in two layers, of which the tilted angle $\theta$ is $45^\circ$ to form cross configuration. The inner layer and outer layer are connected in series.

![Image of double helix coil](image)

**Figure 4.** The structures of the $R_X$ coils for flux pipe-based inductive link.

Table 2 shows the specifications of the simulation models for comparing the performance of the inductive link according to the type of the flux pipe. Aside from the flux pipe models described above, a planar coil in the form of double D (DD), which are applied to conventional IPT systems, was also modeled together for comparative study. In the case of the flux pipe model, the coil size and winding turns were set to be the same, and the same model was used for the $T_X$ pad. In addition, the DD coil was designed to have the same number of turns within the same width and length, and Litz wire with 200 strands at 2.2 mm diameter was used for both the $T_X$ coil and the $R_X$ coil. The litz wire is used by most engineers and researchers for the two coils of wireless power transfer systems. [30–32]. Compensation capacitors connected in series with the coils on the secondary and primary sides were calculated using Equation (2).

**Table 2.** Simulation models for comparative study of inductive link.

| Parameter                  | Type I         | Type II       | Type III      | Type IV       |
|----------------------------|----------------|---------------|---------------|---------------|
| $R_X$ coil topology        | Ideal solenoid | Helix         | Double Helix  | Planar (Double D) |
| Winding Turns of $R_X$ coil| 20             | 20            | 20 (inner 10/outer 10) | 20 (10 x 2 EA) |
| Helix angle                | $0^\circ$      | $45^\circ$    | $\pm45^\circ$ | N/A           |
Table 2. Cont.

| Parameter                              | Type I            | Type II           | Type III          | Type IV           |
|----------------------------------------|-------------------|-------------------|-------------------|-------------------|
| Coil size (width × length)             | 100 × 80 mm       | 100 × 80 mm       | 100 × 80 mm       | 100 × 80 mm       |
| R<sub>X</sub> coil Inductance, L<sub>D</sub> | 6.37 µH           | 7.62 µH           | 7.53 µH           | 8.89 µH           |
| Compensation capacitor, C<sub>S</sub> at secondary side | 550.25 nF         | 459.69 nF         | 465.50 nF         | 394.23 nF         |
| Quality factor, Q<sub>S</sub> @ 85 kHz  | 149.7             | 169.5             | 159.5             | 328.2             |
| TX pad topology                        | Solenoid with ferrite core | Solenoid with ferrite core | Solenoid with ferrite core | Solenoid with ferrite core |
| Winding Turns of TX coil               | 30                | 30                | 30                | 30                |
| Coil size (width × length)             | 100 × 90 mm       | 100 × 90 mm       | 100 × 90 mm       | 100 × 90 mm       |
| Ferrite core size (width × length)     | 100 × 110 mm      | 5 × 110 mm (7 EA) | 5 × 110 mm (7 EA) | 5 × 110 mm (7 EA) |
| TX pad inductance, L<sub>P</sub>       | 145.81 µH         | 38.73 µH          | 90.52 nF          |
| Compensation capacitor, C<sub>P</sub> at primary side | 24.04 nF          | 20 mm             | 2.2 mm            | 200               |
| Output power, P<sub>OUT</sub>          | 1 kW              | 1 kW              | 1.6 kW            | 400 W             |
| Gap distance                           |                   |                   |                   |                   |
| Litz wire dia.                          | 20 mm             |                   |                   |                   |
| Litz wire strands                       | 200               |                   |                   |                   |

3. Characteristics Analysis

3.1. Coupling Coefficient Between Two Coils

One of the most important factors in the performance of an IPT system is the coupling coefficient between two coils. In this study, coupling coefficients according to the types of inductive links were calculated for electromagnetic analysis. Figure 5 shows the simulation results of magnetic field distribution in each model. This analysis was performed in the physical center without the misalignment of the R<sub>X</sub> coil, and the change in the coupling coefficient according to misalignment in the x, y, and z axis directions was simulated. Figure 6 shows the variation of the coupling coefficient with the size of misalignment in each direction. Here, misalignment in the z direction indicates misalignment in the gap direction between the R<sub>X</sub> coil and the TX pad, and x and y directions indicate lateral misalignment in the axial direction and the width direction of the coil, respectively.

As can be seen from the simulation results, the coupling coefficient between two coils in the aligned state is the largest in the conventional DD type. However, in the conventional DD type, as the misalignment increases, the coupling coefficient decreases rapidly. In particular, when the misalignment in the y direction reaches 50 mm, the coupling coefficient becomes almost zero. In the conventional DD type, the coupling coefficient increases when the z misalignment is greater than 40 mm because one of the two symmetrical D coils enters the alignment region again as the size of the misalignment increases.

Helix flux pipe type has high coupling coefficient tolerance for misalignment in y and z directions but low tolerance in the x direction. In particular, the coupling coefficient in the x direction was asymmetrical with respect to the physical origin. This is because the helix coil has an asymmetrical shape with respect to the coil center due to the tiled angle. Therefore, the existing actual flux pipe type has such asymmetrical characteristics around the physical center.

On the other hand, the double helix flux type has a relatively high coupling coefficient and excellent tolerance of the coupling coefficient reduction according to misalignment. Coupling coefficients due to misalignment in the x-direction are asymmetrical, but are much smaller than in helix coils. The asymmetry characteristic of the double helix type is due to the difference in the outer diameter of the inner and outer layers. However, this result shows that the double helix topology can be considered as a solution to the problem of asymmetry according to the misalignment of the actual flux pipe.
Figure 5. The simulation results of magnetic distributions according to inductive link type. (a) Ideal flux pipe, (b) helix flux pipe, (c) double helix flux pipe, and (d) planar coil.

Figure 6. Cont.
3.2. Power Transfer Efficiency of IPT System

Figure 7 shows the calculation results of maximum power transfer efficiency in each model. The reduction rate of the maximum power transfer efficiency due to a misalignment on the y-axis was relatively large for the conventional DD type; specifically, misalignment of 40 mm or more was found to lead to the high reduction effect. Also, this is the lowest maximum power transfer efficiency due to low self-inductance of the $T_X$ pad. On the other hand, the most suitable inductive link for the IPT system was the double helix flux pipe type in terms of the maximum power transfer efficiency and their reduction rate.

To determine the impact of the load resistance on the power transfer efficiency, the coil-to-coil power transfer efficiency at a resonance frequency of 85 kHz for each inductive link model was evaluated. These simulation results are presented in Figure 8. From the simulation results, it is confirmed that the optimal load resistances for the ideal flux pipe type, helix flux type, and planar coil type are 15 $\Omega$ in all cases. On the other hand, the optimal load resistance for the double helix flux pipe type is 20 $\Omega$. The double helix flux pipe type has a relatively constant power transfer efficiency value according to the load resistance.
**Figure 7.** The maximum power transfer efficiency according to the misalignment: (a) x direction misalignment, (b) y direction misalignment, (c) z direction misalignment.
In addition, it is expected that it can be manufactured relatively robustly because it can maintain tolerance against misalignments. All of these models have the same coil size and number of turns, so it is expected that the cost of manufacturing a two-coil system is almost the same. Although not covered in this study, the coils of the flux pipe topology including the DH coil can be manufactured using a traverse winding machine used in existing power transformers, so it is easy to manufacture. Due to the poor misalignment tolerance performance of wireless charging system applying the planar coils, various studies have been conducted on the flux pipe topology with an excellent misalignment tolerance. In this paper, we propose a novel inductive link based on a flux pipe and series-series (SS) compensation network. The proposed flux pipe uses a double helix coil, which improves the coupling coefficient and misalignment tolerance. In the proposed flux pipe topology, two helical coils are tilted at opposite angles of 45° to form a cross configuration. To verify the feasibility of the proposed DH model, the coupling coefficient between two-coils and the power transfer efficiency of the inductive link according to misalignment were analyzed. In addition to the DH coil model, the characteristics of the inductive link models with ideal solenoid coil, helix coil and DD coil were also analyzed. The results show that the proposed model has the best characteristics in terms of the power transfer efficiency and tolerance against misalignments. All of these models have the same coil size and number of turns, so it is expected that the cost of manufacturing a two-coil system is almost the same. Although not covered in this study, the coils of the flux pipe topology including the DH coil can be manufactured by using a traverse winding machine used in existing power transformers, so it is easy to manufacture. In addition, it is expected that it can be manufactured relatively robustly because it can maintain winding tension. The analytical results demonstrate that the proposed DH flux pipe-based inductive link is capable of effective misalignment tolerance performance. However, further research on the applicability of the proposed model is needed, with the fabrication and testing of prototype models.

5. Conclusion

An inductive link including a double helix flux pipe was proposed and analyzed for an IPT system of an EV. The simulation results confirm that the proposed double helix type has the best characteristics in terms of the power transfer efficiency and tolerance against misalignments. At the same time, the double helix flux pipe type also showed an excellent coupling coefficient. This means that the novel flux pipe type proposed in this paper has potential as an inductive link for IPT systems.
of electric vehicles. However, further research on the applicability of the proposed double helix flux pipe is needed through the fabrication and test of prototype models. This study is expected to serve as a reference for performance improvements of IPT systems for electric vehicles.

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