An account is given of the methods of working of Experimental High Energy Particle Physics, from the viewpoint of statisticians and others unfamiliar with the field. Current statistical problems, techniques, and hot topics are introduced and discussed.

1. Particle Physics

1.1. The Subject

Particle Physics emerged as a discipline in its own right half a century ago. It pioneered ‘big science’: experiments are performed at accelerators of increasing energy and complexity by collaborations of many physicists from many institutes. It has evolved a research methodology within which statistics is of great importance, although it has done so without strong links to the statistics community – a fault that this conference exists to remedy. Thus although a statistician will be familiar with the research methods and statistical issues arising in, say, agricultural field trials or clinical testing, they may be interested in a brief description of how particle physicists do research, and the statistical issues that arise.

Particle physics is also known as High Energy Physics and the names are sometimes merged to give High Energy Particle Physics. Whatever it is called, its field of study is all the ‘Elementary’ Particles that have been discovered:

- The 6 quarks (u, d, s, c, b, t)
- The 6 leptons (e, μ, τ, ν_e, ν_μ, ν_τ)
- The intermediate bosons: W, Z, γ, g
- The 100+ hadrons made from two quarks (π, K, D_s(2317)... ) or three quarks (p,n, Λ...) or five quarks (Θ^+...)

This list of proposed particles is limited only by the imagination of the theorists who propose them – which is no limitation at all.

For each species of particle we want to establish:

- Does it exist?
- If it does exist, what are its properties: its mass, its lifetime, its charge, magnetic moment and so on?
- If its lifetime is not infinite, what particles does it decay into? What are the branching fractions to different decay modes? What are the distributions in the parameters (energies and directions) of the particles in the final state? Do they agree with our theoretical models?
- What happens when it collides with another particle? What processes can occur and with what probabilities (expressed as cross sections)? What are the distributions of the parameters of the particles produced? Answers will depend on the target particle and the collision energy.

1.2. Template for an Experiment

To study some phenomenon X, which could be any of the above, a particle physics experiment goes through the following stages:

- Arrange for instances of X
  This may involve a beam of particles, directly from an accelerator or through some secondary system, striking a target; the beam and target particles and the energy are chosen as being favourable for X. It may entail a colliding beam machine like LEP for the Z or BABAR for CP violation in the B system or the LHC for the Higgs. It may be done by producing particles and then letting them decay, as in the studies of CP violation in the K^0 system. An extreme example is proton lifetime studies, where one just assembles...
a large number of ordinary protons (perhaps as hydrogen in water) in suitably low-background conditions deep underground and waits to observe any decays.

For important studies dedicated experiments (even accelerators) are built. For many more, the experimenter utilises data taken with an experiment designed primarily for another purpose but also favourable for $X$. An example is the study of charm mesons at $\text{BaBar}$, Belle and CLEO, for which the primary purpose is $B$ physics.

- Record events that might be $X$
  A detector is built (or an existing detector is utilised). ‘Events’ – interactions or decays – are observed by a whole range of detectors (tracking detectors like drift chambers and silicon detectors, calorimeters that measure deposited energy). Fast logic and/or online computers select the events that look promising, and these are recorded: the phrase ‘written to tape’ is used even though today the recording medium is generally disk storage.

- Reconstruct the measurable quantities of the visible particles.
  The electronic signals are combined and interpreted: points are joined to form tracks, and measurement of their curvature in a magnetic field gives the particle momentum. A calorimeter may give the energy, a Cherenkov counter the velocity. From this emerges a reconstructed ‘event’ as a list of the particles produced, their kinematic quantities (energies and directions) and possibly their identity (as pions or kaons or electrons, etc.)

- Select events that could be $X$ by applying cuts
  Knowing the pattern one is looking for, one can then select the events that contain the phenomenon being studied.

  A key point is that this selection (and also the electronic selection described above) is not going to be perfect. There will always be a selection efficiency which is less than 100%.

  There is also a chance that some of the events that look like $X$ and survive the selection and the cuts are actually from some other process. There will be a background which is greater than zero. Statistical techniques are obviously important for the treatment and understanding of efficiency and background.

- Histogram distributions of interesting variables
  Relevant quantities, sensitive to $X$, are formed from the kinematic variables of the particles detected and measured. These are typically displayed in a histogram, or histograms. (Joint two-dimensional plots are also common. Sometimes, but rarely, the data at this stage is a single number.)

  These distributions are then compared with the theoretical predictions, of which there may be several. One will be the predicted distribution if $X$ is not present. Another may be the prediction if $X$ is present in the amount, and with the properties, predicted by an expected theory such as the ‘Standard Model’ of Particle Physics. There may also predictions obtained within the framework of a particular model, but with one or more parameters adjusted to fit the data.

An example of such a result is shown in Figure 1 (taken from [2]). In the top plot the phenomenon $X$ is the decay of the $B^0$ meson to $D\pi$, in the lower plot the decay to $D^+\pi$. The distributions show the invariant mass, which is the quantity given by

$$M^2c^4 = \left(\sum_i E_i\right)^2 - \left(\sum_i \vec{p}_i c\right)^2$$

where the sums run over the two final-state particles.

If the two observed particles do indeed come from the decay of a $B^0$ particle then this quantity should be $5.28 \text{ GeV}/c^2$, though this is smeared out by experimental resolution. The plots show the predictions of a theory in which this decay does not occur (and all events are background) and also a prediction in which the decay is produced, with a normalisation adjusted to give the best fit to the data. The result of this fit gives the number of signal events, from which the branching ratio can be obtained (though in fact that was not done in this example).

If that looks trivial, a harder example is the decay $B \rightarrow \pi^0\pi^0$, taken from [3] and shown in Figure 2. (To be fair, things are not quite as bad as this 1 dimensional plot implies.)

In this confrontation of theory with experiment, one can then ask: is there any evidence for $X$ or is the null
hypothesis unrefuted? Given that there is $X$, what is the best estimate for the normalisation (and perhaps other) parameter(s) involved in our model for $X$? Are these results compatible with the standard prediction for $X$? These are familiar statistical questions.

1.3. Statistics in HEP

From the above description we can bring out some features of the way statistics is used in HEP.

Firstly, everything is a counting experiment. To measure a branching ratio or a cross section, one counts the number of events produced and observed. To measure the mass of a particle one uses a histogram where the number of entries in each bin is a random Poisson process. (The data of Figure 1 could be used to fit the mass of the $B^0$ meson, were it not already well known.) Poisson statistics is of paramount importance. Even the Gaussian (Normal) distribution plays its main rôle as the large $N$ limit of the Poisson. (There are exceptions to this generalisation, but they occur in the details of the reconstruction of particle quantities.)

This unpredictability is not due to any lack of knowledge on our part: not sampling error, or measurement error, or due to unconsidered effects. It is true and absolute randomness, driven by the fundamental nature of quantum mechanics. We know that, for instance, a $K^0$ particle may decay into two charged pions or two neutral pions, with probabilities of 69% and 31% respectively. That is all we can ever know. A sample of $K^0$ particles will decay to $\pi^+\pi^-$ and $\pi^0\pi^0$ in a ratio of roughly 2:1 even if they are prepared absolutely identically – we have no hope of ever being able to say which ones are more likely to ‘choose’ one path rather than another. Likewise the timing of a decay is absolutely random in that the probability that a particle existing at time $t$ will decay before time $t + \delta t$ is a constant, independent of the value of $t$; there is no ‘ageing’ process.

But the Poisson distributions that result are just like any conventional Poisson process. These and other uncertainties, are (almost always) controlled and understood. These distributions have standard deviations known to be $\sqrt{N}$. The Gaussian used for the signal distributions in Figure 1 is well established (it has a mean of 5.28 and a standard deviation of 0.0025 GeV/c$^2$).

So, in common with the other physical sciences, the distributions involved (signal, backgrounds) are given by functions known up to a few parameters – which can be fitted for. The approach to the data is not descriptive (identifying features, looking for trends) but prescriptive: the distribution is taken as having some functional form, and one has a pretty good idea as to what that functional form is, apart (possibly) from a few adjustable parameters.

1.4. Unused Statistical Methods

A consequence of this knowledge of uncertainty – the fact that we know what it is that we don’t know – is that many techniques commonly used in the broad field of statistics are little used (or not used at all) in particle physics.

Student’s $t$ is unknown. This is a technique used to handle small numbers of values from a distribution of unknown mean and unknown standard deviation, but our uncertainties come from known measurement errors. (If a measurement error is not known, a separate large-number determination is made.) The $F$ test and ANOVA, tools for studying problems with unknown variances, are similarly of little use. The whole experimental design field – Latin squares and similar techniques used to minimise uncontrollable effects – is not needed as such effects are not a problem.

Another set of neglected techniques are those handling Time Series and Markov chains. Changes with time can be relevant in some studies, but it appears in them as another quantity to be measured and histogrammed. The development with time of a particle is basically smooth, punctuated by radical transformations (such as the decay of a particle to two or more lighter ones) which occur at random times.

Non-parametric Statistics are also barely featured, as all these distributions, which are believed to be true idealisations of what ‘really’ happens, or at least good approximations to them, are parametrised.

The notion of a Parent population is not helpful: a sample of particles is taken, but the randomness is (as stated earlier) inherent in the nature of particle behaviour and not produced by the sampling. If there is a parent distribution, it is an infinite set of particles produced under these conditions – all the events we might have seen.

The point here is not that particle physics has nothing to learn from standard statistical techniques. The Statistician has many implements in their toolbox. Different fields of application will call for different tools; some of those heavily used in other fields are of less relevance in this one.
2. Tools

Having seen that particle physics makes little use of some statistical tools, we take a more detailed look at the ones it does utilise.

2.1. Monte Carlo Simulation

Theoretical distributions for the quantities being studied are predicted by quantum mechanics – perhaps with a few unknown parameters – and are often beautiful and simple. Angular distributions may be flat, or described by a few trigonometric terms; masses often follow a Cauchy function (which the particle physicists call the Breit-Wigner), time distributions may be exponential, or exponential with a sinusoidal oscillation.

These beautiful and simple forms are generally modified by unbeautiful and complicated effects (higher-order calculations in perturbation theory, or the fragmentation of quarks into other particles). Furthermore the measurement and reconstruction process that the detector does for the particles is not completely accurate or completely efficient.

The translation from knowing the distributions in principle to knowing them in practice is done by Monte Carlo simulation. Particles are generated according to the original simple distributions, and then put through repeated random processes to describe the theoretical complications and then the passage of particles through the detector, including probabilities for colliding with nuclei in the beam pipe, slipping through cracks in the acceptance, or other eventualities. A complete software representation of all the experimental hardware has to be coded. The effects of the particles on the detector elements is simulated and the information used to reconstruct the kinematic quantities using the same programs that are run on the real data. This provides the full theoretical distribution function that the data is predicted to follow, albeit as a histogram rather than a smooth curve.

These programs are large and slow to run. Significant resources (both people and machines) are put into them. The generation of ‘Monte Carlo data’ is a significant issue for all experiments. Cases are known where data has been taken and analysed but results delayed because of lack of the correct Monte Carlo data.

2.2. The Likelihood

Having the parametrised theoretical description of the distribution means the likelihood function is always known, and it assumes an overwhelmingly important position. Writing this function – where the $x_i$ are the data and $\theta$ the unknown parameter(s) – has the advantage that the minimisation can be done by differentiating and solving the normal equation, which is especially simple if $f$ is linear in $\theta$. However the use of the observed number rather than the predicted number in the denominator

\[ L(x_1, x_2...x_N|\theta) = \prod_{i=1}^{N} P(x_i|\theta) \]

the form $p(x|\theta)$ is totally known, and $L$ (or $\ln L$) follows.

\[ \ln L = \sum_{i} \ln P(x_i|\theta) \]

Figure 3: The log likelihood as a function of a parameter

Having the likelihood function, the Maximum Likelihood estimator is then easy to implement, and is very widely used. Even estimators like least-squares are, at least by some, ‘justified’ as being derivable from Maximum Likelihood. Its (asymptotic) efficiency, and its invariance properties are desirable and useful.

In some cases the ML estimate leads to an algebraic solution but in general, and in complex analyses, the physicist just maps out $\ln L$ for their dataset as a function of $\theta$ and reads off the ML estimator from the peak, as can be done in Figure 3. This also produces an interval estimate as part of the minimisation process. Following the value of $\ln L$ until it falls off by $1\frac{1}{2}$ from its maximum gives the 68% central confidence interval. Strictly speaking this is valid only for large $N$, but this restriction is generally disregarded. Perhaps we should not be so cavalier about doing so.

Maximum Likelihood methods can also be used for functions with several parameters, as illustrated in Figure 4. Confidence regions are mapped out by reading off the likelihood contours. This is done in many analyses and the MINUIT program is widely used in exploring the likelihood and parameter space.

2.3. Fitting Data

Fitting the parametrised curve to the experimental data is done by several techniques.

1) $\chi^2$ using $\sigma^2 = n$ i.e. minimising $\chi^2 = \sum \frac{(y_i - f(x_i|\theta))^2}{n}$ has the advantage that the minimisation can be done by differentiating and solving the normal equation, which is especially simple if $f$ is linear in $\theta$. However the use of the observed number rather than the predicted number in the denominator
is recognised to lead to bias (downward fluctuations get an undue weight) and this cannot safely be used if \( n \) is small. (Actually in many cases what happens is that one of the bins has \( n = 0 \), and the physicist gets divide-by-zero messages and then starts to worry.)

2) \( \chi^2 \) using \( \sigma^2 = f \) i.e. the predicted value rather than the actual number, avoids the bias (and the divide-by-zero problem) but gives nonlinear equations. It still suffers from using a Gaussian probability as an approximation to a Poisson distribution and is thus not the ‘real’ maximum likelihood estimator.

3) ‘Binned Maximum Likelihood’ uses the Poisson likelihood in each bin rather than the \( \chi^2 \). It is therefore a proper Maximum Likelihood estimator. Efficiency is lost (only) if the bins are wider than the structure of the data.

4) Full maximum likelihood does not use binning at all. It can be useful for very small event samples. For large samples it becomes computationally intensive (as there is a sum over events rather than a sum over bins) though with today’s computers this is hardly important. Perhaps a more significant factor for physicists is that it does not have the readily interpretable graphic image given by a histogram and fitted curve.

\[ \chi^2 = \sum_i \left( \frac{y_i - f(x_i|\theta)}{\sigma_i} \right)^2 \]

2.4. Goodness of Fit

Having found a fit, one has to judge whether to believe it. Whether the question is ‘Does the curve really describe the data?’ or ‘Do the data really fit the curve’ depends on one’s point of view.

The likelihood value does not contain the answer to this question. This appears counter-intuitive and many people have wrestled (unsuccessfully) to produce ways that the likelihood can be used to say something about the quality of the fit.

Alternative measures of goodness of fit have never really caught on. The Kolmogorov-Smirnov test is occasionally used – generally misleadingly, in my opinion. This is a totally robust test but pays the price for that by being weak. If you know anything about the data, e.g. that the numerical value of the parameter means something, then a more powerful test should be available. The KS test is being used to certify that distributions are in agreement when a more powerful approach would show up a difference.

2.5. Toy Monte Carlo

The ‘Toy Monte Carlo’ has emerged as a technique made possible by modern computing resources. Having obtained a result, it may be hard or impossible to obtain significance levels or confidence regions in the traditional analytic way, for instance if the likelihood function one is studying does not even plausibly resemble a distorted parabola, but instead some shape with multiple maxima.

As an alternative approach, starting with an estimate \( \hat{\theta}_{exp} \) from the data, say \( \{x_1 \ldots x_N\} \), how can one establish a confidence region? Consider any particular \( \theta \). Use the known \( L(x|\theta) \) to generate a set of \( N \) values of \( x \) – an ‘experiment’. Use this in your estimator (whatever that is) to find a corresponding \( \hat{\theta} \). Repeating many times gives the probability that this \( \theta \) will give an estimate below (or above) the experimental one. This is just what the Neyman construction uses. To find a particular confidence region one has to explore the parameter space until one finds the limits one wants.

3. Topics

Having explained the basic and generally agreed techniques used, there are a number of topics where advances are being made, or which are the subject of heated discussion and argument, or both.

3.1. Bayesian Probability

The religious war which has been waged over the past few years has now cooled – although some isolated zealots remain on both sides. The ‘frequentists’ have come to accept that the use of Bayesian techniques can be illuminating and helpful, and sometimes provide more useful information than a frequentist confidence level, especially for measurements of bounded parameters (e.g. masses). The ‘Bayesians’ are recognising that Bayesian confidence levels will not totally replace the use of frequentist levels, and that
they do have to take on board the issue of robustness (or otherwise) under changes of prior.

A real benefit of this debate has been to bring the subject out into the open. The classic statistics texts \[6, 7\], from which many particle physicists first learned the subject, slide swiftly between the frequentist and Bayesian concepts of probability, never really acknowledging that they are using two very different quantitities.

### 3.2. Small Signals and Confidence Regions

The ‘Energy Frontier’ is a cutting edge of particle physics: new, more powerful, accelerators open up new areas for investigation and new particles are discovered. Another cutting edge is the ‘Luminosity Frontier’: the discovery that processes hitherto thought to be impossible do actually occur, albeit very rarely. The discovery of CP violation \[3\]: that the probability of the decay $K^0_L \rightarrow \pi^+\pi^-$ was not zero but 0.2%, was enormously important despite the smallness of the figure. Many of today’s experiments are looking for phenomena which are known to be exceedingly rare, at the parts-per-million level at best.

Although the implications can be spelt out quite simply and dramatically – ‘If the AMS experiment sees even one $^{127}$C nucleus, our entire view of the universe will change.’ – in practice things are not so cut and dried because of the presence of background. Also one has to be able to handle not just the dramatic discoveries, but the much more frequent useful analyses that make no discovery but push back the limits and the region in which any discovery may be made.

An experiment that sees no events will note the standard result from Poisson statistics that an observed number of zero translates to a limit on the true value of less than 3 events, with 95% confidence. This can then be converted (using the figures for this particular experiment) into a limit on the branching ratio or cross section for the process concerned, and then possibly into a limit on a mass or coupling constant. If there is an expected background for this process equivalent to, say, 0.2 events, then the amount for the branching ratio limit is reduced to 2.8. But this clearly has problems: suppose the predicted background were 3.1 and no events were observed (unlikely but not impossible), what can one then say about the limit?

There has been a lot of activity and discussion recently in this area. Indeed it sparked off the workshop \[8\] of which this conference is the successor. The standard frequentist (Neyman) construction may result in statements about results in the non-physical region (here, a negative number of signal events) which, though statistically correct, appear nonsensical. Bayesian methods avoid this problem, as does the frequentist technique proposed by Feldman Cousins \[9\] which switches smoothly and automatically between quoting central and one-sided confidence regions.

### 3.3. When to Claim a Discovery?

Another area of discussion is over the form of reporting non-zero signals. When the number of signal events is much larger than the expected background, or a fitted parameter is significantly different from the theoretical prediction, then clearly the experiment can claim a discovery. If the numbers or parameter values are compatible, the experiment quotes an upper limit. But there is an area in between where the probability of the null hypothesis giving the result is small enough to be interesting, but not so small as to be completely negligible. The experiment must not be rash, phoning the New York Times with a discovery which turns out to be a statistical fluctuation, nor must it be too cautious or the subject can never progress. Such results are bound to occur – the probability that an experiment will produce a value in this region is by definition small-but-not-negligible, or better. Given the large number of busy experiments reporting results, this is a real problem.

Some experiments have policies such as 4$\sigma$ for ‘evidence for’, 5$\sigma$ for ‘discovery of’ – significance levels are often presented in terms of the equivalent discrepancy in standard deviations. Is it possible to report a two-sided result (as the Feldman Cousins technique will sometimes produce) and yet not claim a discovery? ‘We report with 95% confidence that the branching ratio lies in the range $(2.3 \pm 3.4) \times 10^{-6}$ but we’re not actually claiming to have seen it.’ Such ‘discoveries’ are reported in a way which must be affected by the prior (subjective) probability, in exactly the way the Bayesians describe. Statistically identical data on the decays $B^+ \rightarrow \pi^+\pi^0$ and $B^+ \rightarrow \pi^-\pi^0$ would be reported completely differently.

### 3.4. Blind Analysis

In recent years particle physicists have become aware of practitioner bias. This has been fuelled particularly by reports from the Particle Data Group, which has the job of reporting and combining the measurements of particle properties \[10\], who show how some values change significantly over time, but never by more than one standard deviation. Another source of disquiet was the Electroweak measurements from LEP and the SLC which agree with each other and with the Standard Model far too well with a $\chi^2$ per degree of freedom well below 1 \[11\].

This practitioner bias is against claiming differences from the null hypothesis. The experiment template presented in section \[12\] often continues
• Extract result, usually by fitting parametrised distribution(s) to data.

• Compare your result with that of accepted theory and/or other experiments.

• If it disagrees, look for a bug in your analysis. You will probably find one. Keep searching and fixing until the agreement is acceptable.

The mistake in method is that the experimenter stops looking for bugs when they have agreement, not when they honestly believe that all (substantial) biases are accounted for. To guard against this the data can be ‘blinded’. There are two techniques used, covering two types of situation

• In the extraction of a result, this can be encoded by some unknown offset.

• Choosing the cuts which select the data is done on Monte Carlo data, or on real data in sidebands – regions close to but not actually including the region where the signal is expected. Otherwise the temptation to nudge a cut slightly to include a few more events is too great.

3.5. Systematic Errors

In the early days of particle physics, the 50s and 60s, a typical experiment would get handfuls of events – a few hundred if lucky – from painstaking analysis of bubble chamber pictures. Statistical errors were thus \( \sim 10\% \) and were so large that the effect of systematic uncertainties was generally small.

In the 70s and 80s, the development of counter experiments led to event samples in the tens of thousands. Statistical errors were now at the per cent level, and systematic errors began to be more important.

The current generation of experiments – the Z factory at LEP, the B factories, Deep Inelastic Scattering at HERA – deal with millions of events. Statistical errors were thus \( \sim 0.1\% \) and we have learned how to talk about ‘parts per mille’.

Systematic errors (uncertainties in factors systematically applied in the analysis) can no longer be fudged. The word ‘conservative’ has been grossly overused in this context. It sounds safe and reassuring; in practice it is usually a sign of laziness or cowardice. The experiment perhaps cannot be bothered to evaluate an uncertainty and makes a guess, and then it inflates that guess to cover the possibility that they’ll be caught out, and calls it a ‘conservative’ estimate of the systematic error.

Particle physicists also confuse the evaluation of systematic errors with overall consistency checks. There is bad practice being spread to and between graduate students. They will identify all the calibration constants and parameters that contribute to the final result and vary those by their appropriate error, and fold the resultant variation into the systematic error. This is correct procedure. But they will also vary quantities like cut values, which should not in principle affect the result, by some arbitrary amount and then solemnly fold those resulting variations into the systematic error. This is nonsense. Looking at what happens when you change a cut value is a good and sensible thing: a (say) looser cut will give a higher efficiency and a higher background and thus more observed events, but after correcting for the new efficiency and background the result should be compatible with the original. This is a useful check that one understands what’s going on and that the analysis is consistent. But it does not feed into a numerical uncertainty.

3.6. Unfolding

Measurements of the properties of particles in events are made with finite resolution, so the plots of these quantities, and functions of these quantities, are ‘smeared out’. Events move between histogram bins. Sharp peaks become broad, edges become slopes.

The recovery of the original sharp distribution from the observed one is known as ‘unfolding’. This is an alternative use of the Monte Carlo simulation process: rather than compare the data with a theoretical prediction smeared by Monte Carlo simulation, one compares the original theory with the de-smeared data. Clearly this is preferable, if it can be done, as the unfolding process depends only on the experiment and not on the original theory, and so once unfolded the data can be compared with any prediction.

It looks a simple problem: given an original distribution as a histogram, the probability of migration from any bin \( i \) to any bin \( j \), \( P_{ji} \), can be estimated from a Monte Carlo sample (this includes the probability that it may not be accepted: \( \sum_j P_{ji} \leq 1 \)). The matrix is inverted, and then applied to the data histogram to give the reconstructed original.

Unfortunately it is not at all simple. In the matrix inversion the errors on the \( P_{ji} \) from finite statistics have devastating consequences and produce unrealistic results. There is a lot of activity in handling this in a sensible way, and in investigating other approaches, such as Maximum Entropy techniques.

3.7. Combining Results

The combination of compatible measurements with different errors is straightforward. However results are sometimes incompatible, or marginally compatible. But something must be done with the results, as the community needs a way of using the combined number. Indeed it is the responsibility of the Particle
Data Group [11] to combine measurements and form ‘world average’ results in a meaningful way.

There is also a problem in combining limits. If two experiments report 95% confidence level upper limits of, say, 0.012 and 0.013, how can one combine these two measurements? This question was put forcefully by the Higgs searches at the end of the LEP run. The four experiments reported results separately compatible and possibly marginally suggestive of a signal from a Higgs boson of mass around 114 GeV/c². Did four possibles make a probable? The answer to that statistics question determined whether or not LEP would run another year, at a cost of millions not only in power bills but in its impact on the construction schedule for the LHC. The CERN management decided that the answer in this case was ‘no’. History will be their judge.

In combining experiments the likelihood function contains much more information than a simple limit, or value and error. There is a suggestion that these should be routinely published, and we are probably going to see that happening a lot in the future.

3.8. Multivariate Classification

The classification of events (usually ‘signal’ and ‘background’) and particles (pion, kaon...) by means of a cut on a discriminator variable is a basic hypothesis testing problem. However there may be several variables, each containing useful information, and the best choice will be made by combining these in some way.

The Fisher Discriminant has been re-discovered as a technique which is good if the means of distributions differ between the two samples. The Neural Network (feed-forward ‘perceptron’ configuration) has become a standard item in the toolbox which can handle more general differences, and there are many developments going on in this area.

The use of cuts is deeply engrained. In many cases it is simple and appropriate. However in cases where there are no clean boundaries it may be better to consider all events, weighting them according to their signal-like or background-like nature.

4. Conclusions

I have given several talks on ‘Statistics for Particle Physicists’ but ‘Particle Physics for Statisticians’ has been a new and interesting experience. This has been a very broad view. Particular topics will be considered in detail in the subsequent talks in this conference, in both plenary and parallel sessions. Hopefully the account here will provide you with a map which will help you place them in context.

Acknowledgments

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