Using Self-Contradiction to Learn Confidence Measures in Stereo Vision

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Abstract

Learned confidence measures gain increasing importance for outlier removal and quality improvement in stereo vision. However, acquiring the necessary training data is typically a tedious and time consuming task that involves manual interaction, active sensing devices and/or synthetic scenes. To overcome this problem, we propose a new, flexible, and scalable way for generating training data that only requires a set of stereo images as input. The key idea of our approach is to use different viewpoints for reasoning about contradictions and consistencies between multiple depth maps generated with the same stereo algorithm. This enables us to generate a huge amount of training data in a fully automated manner. Among other experiments, we demonstrate the potential of our approach by boosting the performance of three learned confidence measures on the KITTI2012 dataset by simply training them on a vast amount of automatically generated training data rather than a limited amount of laser ground truth data.

1. Introduction

Many works have demonstrated that machine learning can be greatly beneficial for stereo vision [23, 31, 36, 24, 10]. All these works have one thing in common: They require training data – the more the better.

Previous approaches used three main sources of training data. The first source is manual labeling. While this is the traditional approach in the fields of classification and segmentation (e.g. [5, 33, 29]), it requires hundreds of man-hours even in 2D. Because the task becomes even more taxing in 3D, only very few manually labeled datasets exist in this domain (e.g. [18]). The second source is synthetic data generation [2, 24]. Unfortunately, pure synthetic data generation has not yet reached the level where it generalizes to natural images without an extreme modeling effort. The third source is to record ground truth data with active depth sensors, which is currently the most popular source [32, 7, 21, 27]. If a projector based setup is used [27], the ground truth can achieve a very high accuracy, but the data acquisition takes a lot of time and is restricted to indoor scenes. For outdoor scenes the method of choice is typically the use of a laser scanner [32, 7, 21]. Aside from requiring a non-trivial registration between the laser reconstruction and the recorded images, this method is also subject to a range of assumptions itself. This fact makes a manual removal of obviously incorrect ground truth data necessary for outdoor datasets [7, 21]. Some approaches, like [21], combine these three sources. They combine active sensing with synthetic car models and manual annotation to increase the quality of ground truth data.
None of these methods is easily portable to very specific application areas such as under water reconstruction or 3D reconstruction with micro aerial vehicles. Furthermore, none of these methods shows good scaling properties in the sense of required man-hours per training data.

This motivated us to propose a novel way of generating training data without a synthetic model, active devices or manual interaction. Instead of explicitly generating a ground truth, we compare multiple depth maps of the same scene obtained with the same stereo approach with each other and thus collect positive and negative training data. As input we require a set of stereo images observing a static scene from multiple viewing angles. After computing the relative poses and generating depth maps, we evaluate which parts of the depth maps can likely be trusted, which parts contradict each other and for which parts we simply do not have enough information available to make this decision. This results in a set of partially labeled images, similar to ground truth, which can be used for training (see Fig. 1).

For the evaluation of our method we use three publicly available datasets, which are namely the multi-view stereo dataset of Strecha et al. [32], the Middlebury2014 dataset [27] and the KITTI2012 stereo dataset [7]. On these datasets we demonstrate that the performance of learned confidence measures can be boosted by simply training them on large amounts of domain specific training data, which our approach can cheaply provide.

2. Related Work

To the best of our knowledge, we are the first to approach the topic of stereo training data generation in a self-supervised manner. In order to demonstrate the usefulness of our groundtruth generation, we show that existing stereo vision approaches, which already have been evaluated on one or more of the afore mentioned stereo datasets, can also be successfully trained on our generated data.

Thus, we first give a short overview of the most relevant learning based stereo approaches. While most approaches pose the problem of learning reconstruction errors as a binary classification problem (correct matches/depth values versus incorrect matches/depth values), Kong and Tao [17] propose to use an additional class for failures due to foreground fattening. Using these predicted class probabilities they adjust the initial matching cost. Peris et al. [24] train a multi-class Linear Discriminant Analysis (LDA) classifier to compute disparities together with a confidence map. Žbontar and LeCun [36] improve the matching cost computation by learning a similarity measure between small image patches using a convolutional neural network.

The approaches mentioned above are very specific in their formulation, but many other works use a so called “confidence measure“ as a basis for improving the stereo output. A confidence measure should predict the likelihood of a depth value being correct and is typically computed using image intensities, disparity values and/or matching costs. Some surveys about confidence measures are available in [16, 3, 4]. In the simplest way a confidence measure can be used to remove very likely wrong measurements from the depth map. This process is called sparsification. The most common way for sparsification without training is the left-right consistency check [16]. While this check already detects many outliers, it cannot detect errors caused by a systematic problem of an approach (e.g. foreground fattening). Haeusler et al. [10] showed that ensemble learning of many different features with random decision forests can significantly improve the sparsification performance. Note that confidence measures are also learned in similar fashion in the domain of optical flow, e.g. [20, 6]. Spyropoulos et al. [31] used the confidence prediction as a soft-constraint in a Markov random field to improve the stereo output. In the very recent work of Park and Yoon [23] the confidence prediction is used to modulate the matching cost of a semi-global matcher [15] and thus increase its performance. As the performance of the above mentioned approaches depends on how well the confidence of a measurement can be predicted, the area under the sparsification curve is one of the most important evaluation criteria in this domain [10, 23]. Hence, we found that this criterion is ideally suited to benchmark the quality of our training data generation, aside from comparing it directly to the ground truth. In our experiments, we use three recent approaches [10, 31, 23] that compute confidence measures and analyze the change of performance depending on the used training data (laser ground truth vs. automatically generated training data) on the KITTI2012 dataset [7].

Aside from stereo vision, there exist some works that deal with learning the matchability of features. Some of these works [1, 34, 11] use ground truth data collected by [1]. To generate the ground truth data they use the dense multi-view stereo reconstruction algorithm provided by Gosele et al. [9] and trust this approach to be accurate enough. The problem with applying this approach to dense stereo is that a learning algorithm will try to tune its output to reproduce any systematic error made by [9]. Philbin et al. [25] use SIFT [19] nearest-neighbors together with a RANSAC verification to generate negative and positive training data, whereas Simonyan et al. [30] first compute a homography between images using SIFT and RANSAC and then establish region correspondences using the homography. Hartmann et al. [14] learn the matchability of SIFT features by collecting features that survive the matching stage and those which are rejected as positive and negative training data. All of these approaches focus on a specific type of sparse feature and do not generalize well to dense stereo.
3. Fully Automatic Training Data Generation

The core idea of our training data generation approach is to relax the aim from labeling each pixel as correct/incorrect to labeling them as self-consistent/contradicting. We use the word self-consistent in the sense that depth maps generated with the same algorithm from different view points shall not contradict each other through free space violation or occlusion. Note that the use of different view points is important as the errors in depth maps are in general strongly correlated, if they are generated from the same view point with the same stereo algorithm. In this work we use the observation that this correlation is small when the relative observation angle between two depth maps is large to reduce the influence of systematic errors. The basic steps of our approach are visualized in Fig. 2.

As input our approach requires a set of stereo images with known poses. First, we execute the query algorithm, which yields a set of depth maps (Setup). Then we assess which parts of a depth map are supported by other depth maps with a significantly different observation angle (Stage 1). In the next stage (Stage 2), we then use this support to influence the voting process. In the final stage (Stage 3), we detect outliers which were missed in the previous stage using an augmented depth map. In the remainder of this section, we describe all involved steps in more detail.

3.1. Stage 1: Support Assessment

Given many depth maps of the same scene, we want to separate parts of the scene where many depth maps agree on the structure (consistent parts) from those where they either disagree or we simply do not have enough view points to rule out systematic errors.

In performing this separation, we have to account for two problems. The first problem is that if the camera poses of two stereo pairs are too similar, the depth maps will very likely contain the same systematic error. To remedy this situation, we try to decrease the error correlation in using different observation angles. The second problem originates from the finite precision of cameras, which introduces a depth uncertainty. This means that a measurement with a high uncertainty is not well suited for determining whether a measurement with a lower uncertainty is correct or not. To estimate this uncertainty we use the model proposed by [12]. This model allows us to compute a covariance matrix for each 3D point corresponding to a depth value through first-order backward covariance propagation under the assumption of isotropic Gaussian image noise, which is explained in more detail in [13].

As we aim to produce 2D label images, we address this problem on a per-pixel basis. So for each pixel of a depth map, we first collect the support of other depth maps. A reference depth map is only allowed to express its support for the 3D point \( p_{query} \) associated with a query pixel if it fulfills the following two criteria.

First, the viewpoint shall be sufficiently different. We define that a viewpoint is different enough if the observation angle difference between two stereo pairs is sufficiently large (\( \alpha_{diff} > \alpha_{min} \)). We compute this observation angle as \( \alpha_{diff} = \angle(p_{query_{ref}}, p_{query_{query}}) \), where \( c_k \) is the mean camera center of a stereo pair.

Second, the reference measurement shall be within a fixed theoretical tolerance \( \sigma_{max} \) of the query measurement. For this evaluation we use the Mahalanobis distance based on the covariance matrix with the smaller uncertainty (either reference or query).

In order to avoid being too much biased by a single observation direction, a 3D point fulfilling these criteria is not directly allowed to vote, but instead can activate its corresponding bin depending on the observation angle. We use angular bins of \( \alpha_{min} \) degree, where each activated bin increases the support for the query point by one.

3.2. Stage 2: Consistency Voting

The basic idea of this stage is to let all depth maps vote for the (in)consistency of a query depth map. Similar to works in depth map fusion (e.g. [22]), negative votes are cast by free space violations and occlusions and positive votes are cast by measurements which are sufficiently close to each other (see Fig. 3). Opposed to fusion approaches, we aim for a completely different output. While works in depth
map fusion try to improve/fuse the depth map, we only aim to decide which parts of the depth map cause contradictions and which parts are sufficiently consistent. Furthermore, we have to reduce the influence of systematic errors in the voting scheme, which we achieve with the support of a reference measurement computed in the previous stage. In particular this means that only parts which have a support from at least one significantly different observation angle are eligible for voting.

The proposed voting scheme looks as follows. For casting a positive vote \( v_+ \) a reference measurement has to fulfill two properties. First, it shall be more accurate than the query measurement. We evaluate this property with the largest Eigen value of the corresponding covariance matrix. Second, the reference measurement has to be within a fixed theoretical tolerance of \( \sigma_{\text{max}} \) of the query measurement. For this evaluation we use the Mahalanobis distance based on the covariance matrix of the query 3D point. We define a positive vote as:

\[
v_+ = \sqrt{i_{\text{ref}} \cdot \text{support}_{\text{ref}}} \tag{1}
\]

where \( i_{\text{ref}} \) is the smallest Eigen value of the Fisher information matrix of the reference 3D point. This means that measurements with a low theoretic uncertainty get a higher voting strength, as \( \sqrt{i_{\text{ref}}} = 1/\sqrt{u_{\text{ref}}} \), where \( u_{\text{ref}} \) is the largest Eigen value of the covariance matrix and hence \( \sqrt{u_{\text{ref}}} \) can be interpreted as the standard deviation along the axis of the highest uncertainty.

For casting a negative vote a reference measurement has to fulfill three properties. First, it also has to be more accurate than the query measurement. Second, it has to be outside the fixed theoretical tolerance of \( \sigma_{\text{max}} \). Third, it has to cause a free space violation or occlusion as depicted in Fig. 3. In a free space violation, a reference measurement would block the line of sight of a query measurement (left side in Fig. 3), whereas the other way around would cause an occlusion (right side in Fig. 3). If these properties are met, a negative vote is cast:

\[
v_- = -\sqrt{i_{\text{ref}} \cdot \text{support}_{\text{ref}}} \tag{2}
\]

For each pixel in the query depth map the votes are collected. The label of a pixel with more than zero votes is then set depending on the sign of the final sum of votes.

### 3.3. Stage 3: Outlier Detection

In the previous step, we only allowed measurements with a minimal support from a different observation angle to vote and only then if they are more accurate than the query measurement. This restriction is necessary because otherwise the training data would contain a great percentage of incorrectly labeled samples, i.e. false positives (consistent but incorrect) and false negatives (inconsistent but correct). However, this also causes many regions to be missed in which absolutely no consensus can be reached, because they only contain outliers (e.g. top left corner in Fig. 5). In this stage, we aim to detect these outliers for enhancing our negative training data.

First, we label trivial outliers which either lie behind the camera or do not project into the second stereo camera. For the remaining unlabeled regions we compare the depth values of the query camera to a specially augmented depth map. Our procedure for obtaining this augmented depth map is inspired by the stability-based depth map fusion proposed by Merrell et al. [22]. The main difference is that we do not aim for high performance or even the perfect depth map, but a depth map which rather prefers lower depth values which are sufficiently plausible. We found that underestimating the depth values helps us to keep the number of false negatives (inconsistent but correct) low, while at the same time allowing us to recover many true negatives (inconsistent and incorrect). Further, we avoid any smoothness assumptions to preserve fine objects.

For computing the augmented depth map, we collect all depth values of the other depth maps that would project into a pixel of the query image. Then we sort these depth values and search for the closest depth value which obtains a positive score in a voting scheme. This voting scheme is very similar to the one proposed in the previous stage, but many more depth values will end up with a positive score although they are incorrect.

There are 4 differences to the other voting scheme: (1) Every depth map can vote (without accuracy restrictions), (2) the border between consistent and contradicting vote is set to \( 1/\sqrt{u_{\text{query}}} + 1/\sqrt{u_{\text{ref}}} \cdot \sigma_{\text{max}} \) for all measurements and (4) a depth value has to obtain at least three votes to be considered valid. If no such depth value is found, the original depth is kept.

Using the augmented depth map, we now treat a depth value as a negative sample if the following two criteria are met. First, the query depth value has to be smaller than the depth value of the augmented depth map. Second, the difference between those two depth values has to be larger than \( \sigma_{\text{max}} \cdot 1/\sqrt{u_{\text{augmented}}} \), where \( u_{\text{augmented}} \) stands for the largest Eigen value of the covariance matrix of the augmented measurement if we pretend that it is only visible from the query stereo pair. The final training data is then a combination of the negative samples from this stage with the positive and negative training samples from the previous stage.

### 4. Experiments

In our experiments, we use three publicly available datasets, which are namely the KITTI2012 dataset [7], the Middlebury2014 dataset [27], and the Strecha fountain dataset [32].

The main focus of our experiments is on the KITTI2012 dataset [7] because it is well-suited to demonstrate our ap-
approach and has already been used before for the evaluation of confidence prediction algorithms [10, 23]. The KITTI2012 dataset does not only let us evaluate the coverage and accuracy of our approach, but also lets us highlight the usefulness of our approach in boosting the performance of confidence prediction approaches by simply training them on the automatically generated training data.

4.1. General Setup

For all experiments we used the same set of parameters. The parameter $\sigma_{\text{min}} (= 10^5)$ can be used to adjust the trade-off between coverage and label error. As a general rule, we can say that if one increases this parameter, the false positive rate becomes lower, but at the same time the label coverage decreases as well. The parameter $\sigma_{\text{max}} (= 2)$ can be used to express desired accuracy of a query algorithm as a multiple of the $\sigma$ bound.

As query algorithms, we use two different stereo algorithms. The first algorithm is a Semi-Global Matching (SGM) [15] implementation by Rothermel et al. [26] which uses the census transform for computing the matching cost. As a second algorithm we chose the recently proposed Slanted Plane Smoothing (SPS) approach of Yamaguchi et al. [35]. We chose this approach because it shows a very good performance on the KITTI datasets [7, 21], and gives a completely different output than a SGM (piece-wise planar super pixels vs. unrestricted transitions).

For analyzing the benefit of our approach for learning, we have chosen three different recent approaches [10, 31, 23] which are based on confidence prediction. All three approaches use random forests for the confidence prediction, which made it possible to reimplement them in a common framework. The difference between the approaches lies in which hand-crafted features they feed to the random forest. Ensemble learning [10] uses the peak ratio, entropy of disparities, perturbation, left-right disparity difference, horizontal gradient, disparity map variance, disparity ambiguity, zero mean sum of absolute differences and the local SGM energy, which results through consideration of multiple scales in a feature vector of 23 dimensions. Ground Control Point (GCP) learning [31] uses eight features, which are the matching cost, distance to border, maximum margin, attainable maximum likelihood, left-right consistency, left-right difference, distance to discontinuity and difference with median disparity. Park et al. [23] use a feature vector with 22 dimensions, which contains the peak ratio, naive peak ratio, matching score, maximum margin, winner margin, maximum likelihood, perturbation, negative entropy, left-right difference, local curvatures, local variance of disparity values, distance to discontinuity, median deviations of disparities, left-right consistency, magnitude of image gradient and the distance to border.

For the implementation we used the publicly available random forest framework of Schulter at al. [28]. For training the forest we used the same settings in all our experiments. We used 20 trees with a maximum depth of 20 and a minimum leaf size of 100. For choosing a split function we use the standard entropy and draw 2000 random samples per node and 500 random thresholds per feature channel. For every training setup we balanced the dataset on image basis. This means that every image contributed as many positive training examples as negative examples. For the final evaluation, we always considered the complete image. For obtaining the pose estimation on the KITTI2012 dataset we use [8].

4.2. KITTI Dataset

We use the KITTI2012 dataset [7] to evaluate three properties of our ground truth generation, which are namely accuracy, coverage and training performance. The first two, we obtain by comparing our automatically generated label images to label images produced with the laser ground truth provided for the training dataset. For the SGM [26] data we reach an accuracy of 97.3% (STD: 1.4%) at an average coverage of the laser ground truth of 47.8% (STD: 11.8%). For the SPS [35] data we obtain an accuracy of 95.3% (STD: 5.7%) at an average coverage of 48.6% (STD: 13.4%). Note that the coverage mostly depends on the camera motion.
The ideal case to demonstrate our approach would be a circular motion around an object, whereas no motion will result in no labeled images. As the KITTI dataset contains some sequences with very little motion, this results in a high standard deviation of the coverage.

While accuracy and coverage are relevant, the much more interesting factor is how well the data is suited for training an algorithm. To analyze this factor, we benchmark the change of the confidence prediction performance of three recent confidence prediction approaches, which we further refer to as Ensemble [10], GCP [31] and Park [23].

For benchmarking this performance we evaluate the Area Under the Sparsification Curve (AUSC) as in [16, 10, 23]. A sparsification curve plots the bad pixel rate over the sparsification factor. For drawing the curve the pixels are sorted by confidence values and always the lowest values are removed. The AUSC is a very good indicator for the prediction performance of a confidence measure. Sparsification curves for frame 102 of the dataset are shown in Fig. 4, while further sparsification curves can be found in the supplementary material.

For training on the laser ground truth, we follow the evaluation protocol of [10, 23]. This means that we select the frames 43, 71, 82, 87, 94, 120, 122 and 180 of the KITTI training dataset for training. The labels correct/incorrect are set by comparing the query depth maps with the laser ground truth using the standard three pixel disparity threshold. Further on, we will mark a confidence measure trained on this data with the suffix “Laser”. As our approach requires multiple images that view the same scene, we use the 195 sequences of 21 stereo pairs of the KITTI testing dataset for automatically generating our label images. Further on, we will mark a confidence measure trained on this data with the suffix “Ours”. Example label images can be found in Fig. 5 and the supplementary material. For testing we once again follow the protocol of [10, 23] and evaluate the confidence prediction on the KITTI training dataset minus the eight sequences that were used for training on the laser ground truth. Thus, there is no overlap between training and testing for Laser as well as Ours. Also note that Ours has not seen a single ground truth laser scan. In training, we used all available training samples from the laser ground truth and roughly ten times this number from our automatically generated data. Note that this is less than one percent of all available training data. With this setup our implementation used ~20GB of memory for training.

In Fig. 30 we show the mean, minimum and maximum AUSC values of the three confidence prediction algorithms for all combinations of query algorithm and training data. In Tab. 1 we show the AUSC for each approach divided by the optimal AUSC over all evaluated sequences of the KITTI dataset. In all cases, using our training data resulted in a performance boost. In some cases the AUSC even dropped by 10%. A visual comparison of the difference in the confidence prediction can be found in Fig. 5 and the supplementary material. Note that our training data leads to a smoother confidence prediction with significantly fewer artifacts.

As a matter of completeness, we executed our training data generation only on the eight same sequences that were used for training Laser. One has to note that the coverage of our approach depends on the camera motion and one of the sequences (180) contains no useful motion, which leaves our approach with 7 sequences. Using only this limited amount of training data, the AUSC increased by ~10% for all approaches compared to using the 195 testing sequences. This is not surprising, as each of our training images can be considered as weaker compared to the laser ground truth, in the sense that consistency alone cannot uncover all errors and that the coverage of our labeling depends on the camera motion. But this experiment clearly shows that using ten times more “weak” training samples, which can be cheaply generated with our method, still leads to a better performance than fewer “strong” training samples.
Figure 6. Mean, minimum and maximum AUSC values over the three confidence prediction algorithms (Ensemble [10], GCP [31], Park [23]) for all frames of the KITTI training dataset minus the eight frames used for training. We display all combinations of query algorithm (SGM [26] and SPS [35]) and training data (Laser and Ours). The frames were sorted according to mean AUSC value of Ours. As a baseline method we also show the Left-Right Disparity Difference (LRD). Note that Ours (red) is lower than Laser (blue) in most cases. For SGM, all approaches perform always better than LRD if they are trained on Ours, while if they are trained on Laser they sometimes perform worse (e.g. 142). For SPS stereo, the number of severe errors is significantly higher for Laser than for Ours (compare blue versus red peaks above 160).

4.3. Middlebury Dataset

The Middlebury2014 [27] dataset contains a set of 23 high resolution stereo pairs for which known camera calibration parameters and ground truth disparity maps obtained with a structured light scanner are available. The set is divided into 10 stereo pairs for training and additional 13 stereo pairs that we used for testing. The images in the Middlebury dataset all show static indoor scenes with varying difficulties including repetitive structures, occlusions, wiry objects as well as untextured areas.

Due to the limitation that only stereo pairs and no multi-view sequences are provided, we are not able to evaluate the accuracy performance of our ground truth generation. But we can still evaluate the performance of the confidence measures previously learned on the KITTI to evaluate their generalization performance from outdoor to indoor scenes. Figure 7 shows the resulting AUSC curve for SGM [26] and SPS [35], respectively. In Tab. 2 we show the AUSC over the optimal values.

For all combinations of query algorithm and confidence prediction approach, training on the Middlebury increased the performance compared to training on the KITTI and evaluating on the Middlebury. The percentage of area reduction strongly depends on the used confidence prediction approach. We assume that the large variation in area reduction (3%-30%) is caused by features which are very setup specific (e.g. distance to border). Despite the large reduction variation, all approaches benefit from training on the
Middlebury rather than the KITTI. This means that tuning towards a special setup can make a large difference in performance.

4.4. Strecha Dataset

To further demonstrate the value of our approach, we analyze the sparsification performance in a completely different setup. For this experiment we used the multi-view stereo dataset of Strecha et al. [32]. This dataset provides images together with camera poses and two ground truth meshes. From the two available meshes, the Herz-Jesu mesh is a good example that also active sensors have their limitations. In this mesh all the thin structures (hand rails and bars) are simply missing. As these errors would cause problems in the evaluation, we only used the second dataset (Fountain), which does not contain any thin structures. This dataset consists of 11 images aligned to the ground truth mesh. For this experiment we split the images into a training set containing 3 image pairs and a test set with 2 image pairs. The training pairs are made of images 0+1, 4+5 and 8+9 and the testing pairs of 2+3 and 6+7. Each pair was then rectified using [26]. As the SPS implementation [35] failed to produce any reasonable output on this kind of data, we limit this experiment to the SGM [26] reconstruction.

In this setup our ground truth generation reached an accuracy of 95.1% (STD: 2.6%) at a coverage 30.4% (STD: 5.0%). In Fig. 8 we show the resulting two sparsification curves and the AUSC reduction statistics in Tab. 3. All combinations of query algorithms and confidence prediction approaches performed better trained on the Middlebury than on the KITTI. In all cases the performance was further increased by tuning them specifically to this scene in using our automatically generated training data.

5. Conclusion

In this paper we present a novel way to train confidence prediction approaches for stereo vision in a cheap and scalable manner. We collect positive and negative training data by analyzing the consistency between depthmaps that observe the same physical scene. Consistency is a necessary but not sufficient criterion for correctness. On the one hand, this means that consistency is perfectly suited for unveiling incorrect depth values and thus to collect negative training data. On the other hand, it can never be guaranteed that all incorrect depth values are detected through consistency alone, as they can be consistent and incorrect at the same time. To keep the number of incorrect samples in the positive training data low, we only consider parts of the scene which have been viewed from significantly different observation angles for the generation of positive training data. In our experiments, we demonstrate that the resulting training data can be a great benefit for learning-based confidence prediction. On the KITTI2012 dataset, the amount and diversity of our training data allowed us to improve the average confidence prediction performance of three different approaches by 1 to 10% without changing the algorithms themselves. Further, we demonstrated that all three confidence prediction approaches can significantly benefit from learning application specific properties. With our approach, these specific properties can be learned at low cost; even for applications, such as aerial or under water robotics, that typically lack ground truth data.
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A. Supplementary Material

Figures 9, 10 and 11 are extensions to Fig. 5 in the original paper. These figures each show the sparsification curves for three frames of the KITTI2012 dataset [7]. To give a fair overview of good and bad examples, we ranked the frames depending on the benefit of our training data. As we ran multiple combinations of query algorithm (SGM [26] and SPS [35]) and confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]), we decided to base the ranking on the combination with the lowest total Area Under the Sparsification Curve (AUSC) which turned out to be "SGM-Park" (see Tab. 1 in the original paper). Thus, we used the ratio $\frac{AUSC_{SGM-Park-Ours}}{AUSC_{SGM-Park-Laser}}$ for ranking the frames of the KITTI training dataset in ascending order. Based on this ranking we selected the three best frames (Fig. 9), the three frames around the median index (Fig. 10) and the three worst frames (Fig. 11).

For each of these nine frames we show two additional figures (one for SGM [26] (Fig. 4-12) and one for SPS [35] (Fig. 13-21)). Each of these figures shows the RGB input image, the depth image produced by the query algorithm (SGM or SPS), the label images generated with the laser ground truth [7] and with our approach, as well as the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser [7] and Ours).

For the label image generation, note that the amount of generated positive training data is strongly influenced by the camera motion. We require at least one reference measurement which is more accurate than the query measurement and has a minimum relative observation angle of at least $10^\circ$ (compare Fig. 12 and Fig. 17). This leads to a low coverage in the middle of the road, while on the side of the image the labels are more dense.

For the confidence prediction, note that the prediction output trained on our label images (Ours) is less noisy and impact of the distance to border features becomes smoother (e.g. Fig. 12 left margin and bottom right corner of the image). It seems that the random forests over-fit if we only use the limited amount of label images generated with the laser ground truth. In contrast, our more diverse training data reduces the chance of over-fitting, which in turn leads to an improved overall prediction performance.

As a matter of completeness, Figure 30 shows a different version of Fig. 6 in the original paper. While Fig. 6 in the original paper shows the mean, minimum and maximum values across the three confidence prediction approaches (Ensemble [10], GCP [31], Park [23]), Fig. 30 shows each approach individually. The sequences in Fig. 30 were sorted by the optimal AUSC values.
Figure 9. Sparsification curves for the three best frames with (102, 56, and 0) of the KITTI training dataset. The ranking was obtained by the ratio $AUSC_{SGM-Park-Ours}/AUSC_{SGM-Park-Laser}$. We display all combinations of query algorithm (SGM [26] and SPS [35]), confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). As a baseline method we also show the Left-Right disparity Difference (LRD).
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Figure 10. Sparsification curves for the three median frames (85, 126, 88) of the KITTI training dataset. The ranking was obtained by the ratio $AUSC_{SGM-Park-Ours}/AUSC_{SGM-Park-Laser}$. We display all combinations of query algorithm (SGM [26] and SPS [35]), confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). As a baseline method we also show the Left-Right disparity Difference (LRD).
Figure 11. Sparsification curves for the three worst frames (151,35,42) of the KITTI training dataset. The ranking was obtained by the ratio $AUSC_{SGM-Park-Ours}/AUSC_{SGM-Park-Laser}$. We display all combinations of query algorithm (SGM [26] and SPS [35]), confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). As a baseline method we also show the Left-Right disparity Difference (LRD).
Figure 12. Visual comparison of outputs for frame 0 and SGM [26] as query algorithm (rank 3 - best). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 13. Visual comparison of outputs for frame 35 and SGM [26] as query algorithm (rank 185 - worst). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 14. Visual comparison of outputs for frame 42 and SGM [26] as query algorithm (rank 186 - worst). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 15. Visual comparison of outputs for frame 56 and SGM [26] as query algorithm (rank 2 - best). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 16. Visual comparison of outputs for frame 85 and SGM [26] as query algorithm (rank 92 - median). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 17. Visual comparison of outputs for frame 88 and SGM [26] as query algorithm (rank 94 - median). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 18. Visual comparison of outputs for frame 102 and SGM [26] as query algorithm (rank 1 - best). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 19. Visual comparison of outputs for frame 126 and SGM [26] as query algorithm (rank 93 - median). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 20. Visual comparison of outputs for frame 151 and SGM [26] as query algorithm (rank 184 - worst). Top row: RGB input image and SGM [26] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 21. Visual comparison of outputs for frame 0 and SPS [35] as query algorithm (rank 3 - best). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 22. Visual comparison of outputs for frame 35 and SPS [35] as query algorithm (rank 185 - worst). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 23. Visual comparison of outputs for frame 42 and SPS [35] as query algorithm (rank 186 - worst). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 24. Visual comparison of outputs for frame 56 and SPS [35] as query algorithm (rank 2 - best). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 25. Visual comparison of outputs for frame 85 and SPS [35] as query algorithm (rank 92 - median). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 26. Visual comparison of outputs for frame 88 and SPS [35] as query algorithm (rank 94- median). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 27. Visual comparison of outputs for frame 102 and SPS [35] as query algorithm (rank 1 - best). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 28. Visual comparison of outputs for frame 126 and SPS [35] as query algorithm (rank 93 - median). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 29. Visual comparison of outputs for frame 151 and SPS [35] as query algorithm (rank 184 - worst). Top row: RGB input image and SPS [35] depthmap. The color in the depth images ranges from blue (far away) to red (very close). Second row: Label images computed with laser ground truth and with our approach. In the label images the color green stands for positive samples, red for negative and blue is ignored during training and evaluation. In the remaining rows, we display the confidence prediction output for all combinations of confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). The color ranges from black (low confidence) to white (high confidence).
Figure 30. Area under the Sparsification Curve (AUSC) values for all frames of the KITTI training dataset minus the eight frames used for training. The frames were sorted according to the optimal area under the curve value. We display all combinations of query algorithm (SGM [26] and SPS [35]), confidence prediction algorithm (Ensemble [10], GCP [31], Park [23]) and training data (Laser and Ours). As a baseline method we also show the Left-Right disparity Difference (LRD).