DFT study of single water molecule adsorption on the (100) and (101) surfaces of KH$_2$PO$_4$

Lei Zhang, Yulin Wu, Yao Liu* and Hui Li

Potassium dihydrogen phosphate (KH$_2$PO$_4$; KDP) is a widely used non-linear optical material. A critical issue associated with KDP crystals is that the water molecules in the environment inevitably adhere to the surface and affect the surface electronic and physical properties. In order to understand how water interacts with the surface, the adsorption of a single water molecule on the external surfaces of a KDP crystal, including (100) and (101) surfaces, was theoretically investigated based on density functional theory (DFT) method. The most favorable adsorption sites on both surfaces were considered based on the adsorption energy. The electron density difference and partial density of states were calculated to analyze the bond formation during the adsorption process. It was found that the water molecule can be adsorbed in two different ways—forming two hydrogen bonds with the O and H atoms on the surface or forming a hydrogen bond and an O–K chemical bond with the O and K atoms on the surface. We also found that the surface atoms and the pulling effect between two high potential states on the surface play a dominating role in the adsorption process.

1. Introduction

Potassium dihydrogen phosphate (KH$_2$PO$_4$; KDP) is a widely used non-linear optical material with large electro-optical and nonlinear optical coefficients and a high laser damage threshold.\textsuperscript{1–5} It has wide practical applications in laser frequency converters, electro-optic modulators, optical switches and other high technology fields owing to its unique properties.\textsuperscript{6,7}

Large-scale KDP crystals that meet the need of high power laser devices for large size frequency doubling crystals are mainly grown from its saturated aqueous solution.\textsuperscript{8–10} The growth of crystals takes place at the interface between the crystal and the solution, and the atomic structure at this interface plays a primary role in the structure and morphology of the crystal. Thus, many people have studied the structure of the interface. For example, Vries\textsuperscript{11} found that the \{101\} faces of KDP crystal in solution are terminated by a layer of K$^+$ ions and not by H$_2$PO$_4^-$ groups. Reedijk \textit{et al.} studied interface-induced ordering in the first four layers of water molecules through X-ray diffraction. They found that the first two layers behave like ice and are strongly bound to the surface.\textsuperscript{12} KDP crystal is also fragile, thus it is extremely difficult to machine via traditional machining methods. Owing to its water-soluble property, micro water dissolution machining method and micro-deliquescent polishing method have been applied to machine KDP crystals.\textsuperscript{13,14} The dissolution and deliquescent taking place at the surface of the KDP crystals improved the machining quality of KDP optical crystals. Besides the producing and machining processes, the application and storage of KDP are also strongly affected by water. To minimize the Fresnel losses from the optical surface, the KDP surface is usually covered with a sol–gel coating.\textsuperscript{15} However, people found that etch pits can develop at the KDP surface beneath the coating after exposure to ambient humidity.\textsuperscript{16} Water adsorbed from the environment into the coating contacts the KDP crystal surface, causing etch pits nucleation at high undersaturation.\textsuperscript{17}

As we can see, during the producing, machining and application processes, the adsorption of water can have a significant influence on the surface electronic and physical properties of KDP crystals. Therefore, to control the influences of water adsorption, it is essential to understand the interaction between water and KDP crystal surfaces. So far, researchers have mainly focused on two aspects of this issue. One is the structure of the KDP surface in aqueous solution, where they found the K$^+$ ions termination at the \{101\} faces\textsuperscript{18} and the growth morphology of the \{100\} faces.\textsuperscript{18} The other one is the structure of the liquid part of the interface where they found the liquid order at the interface\textsuperscript{13} and a strongly hydrogen bound water layer close to the KDP surface.\textsuperscript{19,20} However there are very few theoretical studies of the adsorption of water molecules on KDP surfaces, while this kind of study has been a research hotspot in other optical materials. For example, water adsorption on TiO$_2$ was investigated by \textit{ab initio} study, showing that molecular adsorption is more favorable than dissociative chemisorption.\textsuperscript{21} The adsorption of water on the potassium sodium tantalite niobate (KNTN) (001) surface was studied by Wang, who revealed the...
energetically favorable configurations for water monomer adsorption.\textsuperscript{22} Giordano \textit{et al.} studied water molecules on the MgO (100) surface, finding the first theoretical evidence of water dissociation on the perfect MgO (100) surface.\textsuperscript{21}

Overall, there are urgent realistic and theoretical needs for the study of the interaction between water molecules and KDP surfaces. In this paper, we are trying to study where a water molecule can be adsorbed more stably on the (100) and (101) surfaces and the differences in how the water molecule is adsorbed on the two surfaces of a KDP crystal. This would help us understand the nature of the interaction between a water molecule and the surfaces of a KDP crystal, and guide us to produce, machine and protect KDP crystal more effectively.

2. Computational details

KDP has a \textit{I}4\textit{1}2\textit{d} space group and crystal lattice parameters of \(a = b = 7.453\ \text{Å}, c = 6.973\ \text{Å}.\)\textsuperscript{24} First, a unit cell of bulk KDP crystal was generated and then optimized. When growing from aqueous solution, two different surfaces are observed on the morphology of the KDP crystal—the (100) and (101) surfaces. Thus, these two surfaces were chosen to be calculated in our work (see Fig. 1(c)). When cleaving the (101) surface, there are two possible ways: one produces a cation (K\(^+\))-terminated surface and the other produces a dihydrogen phosphate (\(\text{H}_2\text{PO}_4^-\))-terminated surface. According to the work by Vries, which indicated K\(^+\) termination at the (101) surface of KDP,\textsuperscript{11} only the K\(^+\)-terminated surface was considered in our calculations. The KDP (100) and (101) surfaces were modeled by a slab of three layers (1 \(\times\) 1 unit cell along the \(x\) and \(y\) directions) in the \(z\)-direction. The thickness of a single layer equals the interplanar distance of the (100) and (101) surfaces. A vacuum spacing in the \(z\)-direction of 30 Å was also used to avoid the influence of periodic boundary conditions (\(x\), \(y\) and \(z\) direction).

All DFT calculations\textsuperscript{25} on the KDP surfaces were carried out using the CASTEP code.\textsuperscript{26} The exchange–correlation potential used in the calculations was the Perdew–Burke–Ernzerhof\textsuperscript{27} (PBE) form of the generalized gradient approximation (GGA).

The electron–ion interactions were described by ultrasoft pseudopotential\textsuperscript{28} (USP). Geometry optimization was carried out using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) scheme.

To describe the dispersion interactions, a semi-empirical correction using the Grimme method\textsuperscript{29} was adopted. To get converged results and reasonable computation time, a plane-wave energy cutoff of 400 eV was used for geometric optimization, which took the most time of the calculations. To get results of high accuracy, a higher cutoff of 680 eV was used for electronic structure calculations. A \(3 \times 3 \times 1\) \(k\)-point grid was used in the self-consistent calculations. The convergence tolerances for energy and force were \(2 \times 10^{-5}\) eV per atom and 0.05 eV Å\(^{-1}\) in the self-consistent calculations, respectively.

3. Results and discussion

In this paper, \(O_W\) and \(H_W\) represent the oxygen atom and hydrogen atoms in a water molecule, respectively. \(O_p\) and \(H_p\) mean the oxygen atom and hydrogen atoms in the related phosphate group, respectively.

The initial adsorption positions of the (100) surface and the (101) surface are shown in Fig. 1(a) and (b), respectively. On the (100) surface, positions \(e\) and \(f\) represent the P top and K top sites, respectively. Positions \(g\) and \(h\) in at the middle sites of two different P–K bridges. Position \(i\) is in the middle site of the K–K bridge. On the (101) surface, positions \(m\) and \(n\) represent the K top and O top sites, respectively. Positions \(o\) and \(p\) are at the middle sites of two different O–K bridges (at position \(o\) the length of the O–K bridge is 2.60 Å, while at position \(p\) the length is 4.36 Å which is significantly longer). Position \(q\) is at the middle site of the K–K bridge. Owing to the symmetry of the (100) and (101) surfaces, these initial positions can represent most of the typical adsorption positions on the two surfaces.

We set the adsorption energy as a criterion to determine the stability of the adsorption. It was calculated from the following equation:\textsuperscript{10,11}

\[
E_{\text{ads}} = E_{\text{slab}}\left(\frac{\text{H}_2\text{O}}{\text{KDP}}\right) - E_{\text{slab}}(\text{KDP}) - E_{\text{H}_2\text{O}}
\]

where \(E_{\text{ads}}\) is the adsorption energy of a water molecule on the KDP surface. \(E_{\text{slab}}\left(\frac{\text{H}_2\text{O}}{\text{KDP}}\right)\) is the total energy of the water–KDP adsorption system. \(E_{\text{slab}}(\text{KDP})\) is the energy of a clean KDP surface. \(E_{\text{H}_2\text{O}}\) is the energy of an isolated water molecule.

The adsorption energies given on positions of the KDP (100) and (101) surfaces are shown in Table 1. According to the adsorption energy of the water molecule at different positions, we get the two most stable configurations of a single water molecule adsorbed on the (100) surface. They are position \(e\) (P top site) and position \(h\) (P–K bridge site). On the (101) surface, the two positions where a water molecule can be adsorbed more stably are position \(o\) (O–K bridge site) and position \(p\) (O–K bridge site). It can be seen that on the (101) surface, the most

![Fig. 1 Initial adsorption positions on the KDP (100) surface (a) and (101) surface (b). (c) The idealized KDP crystal with two growth faces, the (101) and the (100). Dark purple balls represent potassium atoms. Light purple balls represent phosphorus atoms. Red balls represent oxygen atoms. Hydrogen atoms are represented by white balls.](image-url)
stable adsorption sites are both O–K bridge positions while on the (100) surface, a single water molecule can be adsorbed more stably not only at the P–K bridge position but also at the P top position.

The adsorption of a water molecule on the surface of materials always results in structure changes within the water molecule. We compared the interatomic distances and angle of an isolated water molecule and an adsorbed one at the most stable adsorption sites in Table 2. It is clear that at all the adsorption sites, the OH bond of the water molecule that is near to the surface is lengthened (by 0.015 Å to 0.027 Å) after the adsorption process while the OH bond that is far from the surface contracts slightly (by 0.001 Å to 0.005 Å). In addition, the adsorption process results in an increase in the H_W–O_W–H_W bond angle of the water molecule. It could be expected that some electron density may be transferred between the water molecule and the KDP (100) and (101) surfaces, as could be validated from our electron density difference analysis.

### Table 2

| Structure | Isolated | Position e | Position h | Position o | Position p |
|-----------|----------|------------|------------|------------|------------|
| d(OH)(1) (Å) | 0.978 | 0.993 | 0.993 | 1.005 | 1.002 |
| d(OH)(2) (Å) | 0.978 | 0.977 | 0.976 | 0.973 | 0.975 |
| ∠H_W–O_W–H_W (degree) | 104.503 | 105.756 | 105.819 | 107.278 | 105.936 |

3.1. Adsorption of an isolated water molecule on the (100) surface

The geometries of water molecule adsorption at positions e and h on the KDP (100) surface are shown in Fig. 2(a) and (b), respectively. The details of the bond lengths, bond angles and adsorption energy are shown in Table 3. It can be observed that, at position e, one H atom of the water molecule is pulled toward the O atom of the phosphate group (d_{H_w–O_p} = 1.91 Å and ∠O_W–H_W–O_P (shown as ∠1 in Fig. 2) = 147.0°) and the O atom of the water molecule is drawn near to the H atom of the phosphate group (d_{H–O_p} = 1.87 Å and ∠O_p–H_P–O_W (shown as ∠2 in Fig. 2) = 162.2°). The geometry of the water molecule adsorption at position e suggests that two hydrogen bonds (O_W–H_W–O_P) and an O_W–K chemical bond formed during water molecule adsorption at position h.

Electron density difference maps have been used to provide a deeper understanding of the electron density transfer while the water molecule is adsorbed on KDP surface. The electron density difference Δρ is defined by the following equation:

$$\Delta \rho = \rho_{\text{lab}}(H_2O_{\text{KDP}}) - \rho_{\text{lab}}(KDP) - \rho_{\text{H}_2O}$$

where $\rho_{\text{lab}}(H_2O_{\text{KDP}})$, $\rho_{\text{lab}}(KDP)$ and $\rho_{\text{H}_2O}$ are the electron densities of the water–KDP adsorption system after adsorption, the clean KDP surface and the free water molecule before adsorption, respectively. To get a clear picture of the difference in electron density, slices are made through related atoms (at position e shown in Fig. 3(a): slice 1 through H_p and O_w and slice 2 through H_w and O_w; at position h shown in Fig. 3(b): slice 3 through H_w and O_p and slice 4 through O_w and K). It clearly exhibits an increase of electron density between H_w and O_p and between O_w and H_p (see Fig. 3(a)). Such charge distribution illustrates that two hydrogen bonds are formed between the water molecule and the neighbouring phosphate group. Fig. 3(b) shows an increase of electron density between H_w and O_p, which indicates that a hydrogen bond formed at position h. Meanwhile, the electrons of the K atom transfer to the neighboring O atoms of the water and phosphate group, which indicates an O–K chemical bond formed during the adsorption process.
The atomic partial densities of states (PDOSs) of selected atoms of the water molecule and the surface were calculated to study the interaction between the functional atoms on the surface and the water molecule, as shown in Fig. 4. At position e, the resonance peaks between HW 1s states and OP 1s and 2p states are at energies of $-20.2$ eV, $-6.5$ eV and $-2.8$ eV, respectively. The resonance peaks between the OW 2p states and the HP 1s states are in a wide range from $-8.9$ eV to $-2.0$ eV. These resonance peaks can be attributed to the formation of hydrogen bonds. As mentioned above, at position e, $d_{\text{HW-OP}} = 1.87$ Å is shorter than $d_{\text{HW-OW}} = 1.91$ Å and we noticed that the two states between HP and OW have more similar shapes than that between HW and OP, which may indicate that the hydrogen bond between HP and OW is stronger.

Fig. 4(c) shows that, at position h, the resonance peaks between the HW 1s state and OP 1 and 2p states are at energies of $-21.8$ eV, $-6.0$ eV and $-2.0$ eV, respectively. The resonance peaks between the OW 2p states and the HP 1s states are in a wide range from $-8.9$ eV to $-2.0$ eV. These resonance peaks can be attributed to the formation of hydrogen bonds. As mentioned above, at position h, $d_{\text{HW-OP}} = 1.94$ Å is shorter than $d_{\text{HW-OW}} = 1.91$ Å and we noticed that the two states between HP and OW have more similar shapes than that between HW and OP, which may indicate that the hydrogen bond between HP and OW is stronger.

Table 3 The details of bond lengths, bond angles and adsorption energy of single water molecule adsorption at positions e and h on the KDP (100) surface

| Structure | $E_{\text{ads}}$ (eV) | $\angle \text{OW-HW-O}_\text{p}$ (degree) | $\angle \text{OP-HP-O}_\text{w}$ (degree) | $d_{\text{OW-K}}$ (Å) | $d_{\text{HW-OP}}$ (Å) | $d_{\text{HP-OW}}$ (Å) |
|-----------|-----------------|-------------------------------|-------------------------------|-----------------|-----------------|-----------------|
| Position e | $-0.57$         | 147.0                         | 162.2                         | —               | 1.91            | 1.87            |
| Position h | $-0.47$         | 154.1                         | —                             | 3.01            | 1.84            | —               |

Fig. 3 Electron density difference maps between the water molecule and the KDP (100) surface at position e (a) and position h (b). Blue and red colors represent depletion and accumulation of electron density, respectively. Positive values indicate accumulation of electron density. Negative values correspond to depletion of electron density.
18.2 eV, −6.2 eV and −2.5 eV, respectively. Like the two states between $H_W$ and $O_P$ at position $e$, their shapes are not completely similar. One reason may be that the hydrogen bond between $H_W$ and $O_P$ is relatively weak. The other reason may be that the $O_P$ is bonded tightly to other atoms on the KDP surface, thus the peaks in the PDOS of $O_P$ are not only reflecting the bonding between $H_W$ and $O_P$ but also reflecting the bonding with other atoms on the surface. There are two main resonance peaks at energies of −17.5 eV and a wide range from −9.5 eV to 0 eV between the $O_W$ 2p states and the $K$ 2p states, see Fig. 4(d), which reveals that the interaction between the $O_W$ and the surface $K$ atom is relatively strong.

### 3.2. Adsorption of an isolated water molecule on the (101) surface

Geometries of water molecule adsorption at positions $o$ and $p$ on the KDP (101) surface are shown in Fig. 5(a) and (b) respectively. The details of bond lengths, bond angles and adsorption energy are shown in Table 4. As shown in Fig. 5, the geometries of water molecule adsorption at positions $o$ and $p$ on the KDP (101) surface are quite similar. Taking the geometry at position $o$ as an example, one $H$ atom of the water molecule is pulled toward the $O$ atom of the phosphate group, indicating a strong interaction between $H_W$ and $O_P$. The short $H_W$–$O_P$ distance and the large $O_W$–$H_W$–$O_P$ angle (shown in Table 4) imply that this interaction is the hydrogen bond ($O_W$–$H_W$–$O_P$) formed during the adsorption process. Meanwhile, the $O$ atom of the water molecule is attracted to the $K$ atom of the surface, which suggests that an $O_W$–$K$ chemical bond is formed during the adsorption process at position $o$. The similar geometry at position $p$ leads to the same conclusion that a hydrogen bond ($O_W$–$H_W$–$O_P$) and an $O_W$–$K$ chemical bond are formed when a single water molecule is adsorbed at position $p$.

The electron density difference maps between the water molecule and the KDP (101) surface at positions $o$ and $p$ are shown in Fig. 6(a) and (b), respectively. In addition, slices are made through related atoms (at position $o$ shown in Fig. 6(a): slice 5 through $H_W$ and $O_P$ and slice 6 through $O_W$ and $K$; at position $p$ shown in Fig. 6(b): slice 7 through $H_W$ and $O_P$, slice 8 through $O_W$ and $K$) to show the difference in the electron density.
density clearly. The electron density transfer of these two positions is similar too. The electrons of $H_W$ transfer to the neighbouring $O_P$, which indicates that a hydrogen bond is formed. Meanwhile, the electrons of the K atom transfer to the neighbouring $O_W$, which indicates that an $O$–$K$ chemical bond is formed during the adsorption process.

We also calculated the PDOSs of the selected atoms, as shown in Fig. 7. At position o, as shown in Fig. 7(a) and (b), the resonance peaks between the $H_W$ 1s states and the $O_P$ 1s, 2p states are at energies of $-20.5$ eV and $-6.7$ eV and range from $-3.8$ eV to $-1.5$ eV. These resonance peaks might be attributed to the formation of a hydrogen bond. There are two main resonance peaks at energy of $-18.5$ eV and a wide range from $-8.6$ eV to 0 eV between the $O_W$ 2p states and the K 2p states, which reveals a strong interaction between $O_W$ and K exposed on the surface.

### Table 4
Details of the bond lengths, bond angles and adsorption energies of single water molecule adsorption at positions o and p on the KDP (101) surface

| Structure | $E_{ads}$ (eV) | $\angle O_W$–$H_W$–$O_P$ (degree) | $\angle O_P$–$H_P$–$O_W$ (degree) | $d_{O_w-K}$ (Å) | $d_{H_w-O_p}$ (Å) | $d_{H_P-O_W}$ (Å) |
|-----------|---------------|-------------------------------|-------------------------------|----------------|----------------|----------------|
| Position o | $-0.60$       | 156.1                         | –                            | 2.67          | 1.67          | –              |
| Position p | $-0.63$       | 173.3                         | –                            | 2.79          | 1.77          | –              |

Fig. 6  Electron density difference maps between the water molecule and the related phosphate group at position o (a) and position p (b) on the KDP (101) surface. Blue and red colors represent depletion and accumulation of electron density, respectively. Positive values indicate accumulation of electron density. Negative values correspond to depletion of electron density.
At position p, shown in Fig. 7(c) and (d), the resonance peaks between the HW 1s states and the OP 1s, 2p states are at energies of $-20.5$ eV, $-6.7$ eV and $-3.4$ eV, respectively. Compared with the PDOSs at position o, the less similar shape of the resonance peaks indicates that the hydrogen bond is weaker than that at position o. We also noticed that $d_{HW-OP}$ is larger at position p (1.77 Å) than that at position o (1.67 Å). The longer bond length also indicates that the hydrogen bond at position p is weaker than that at position o. The resonance peaks between OW 2p states and neighbor K 2p states are at an energy of $-19.1$ eV and a wide range from $-8.7$ eV to 0 eV, which proves the formation of O–K chemical bond. Because the distance between OP and K on the (101) surface at position p is longer than that at position o, when a hydrogen bond and an O–K chemical bond are formed, the two bonds have to be stretched to adapt to the longer distance between OP and K, making both bonds weak.

After the comparison and analysis of the adsorption behaviors of a water molecule and two typical surfaces of KDP, we found different interactions between the water molecule and the KDP surfaces. On the KDP (100) surface, the water molecule may form two hydrogen bonds with the neighbor phosphate group (position e) or form an O–K chemical bond with the neighbor K atom and a hydrogen bond with the neighbor phosphate group (position h) during the adsorption process. While on the KDP (101) surface, the water molecule can only be adsorbed by forming an O–K chemical bond and a hydrogen bond. This difference is caused by the different structures of the (100) and (101) surfaces of the KDP crystal. There are three kinds of elements (K, O and H atoms of the phosphate groups) exposed on the (100) surface, making it possible to form two hydrogen bonds ($OW–HW⋯OP$ and $OP–HW⋯OW$) when a water molecule gets close to a phosphate group. However, on the (101) surface, there are only two kinds of atoms (K and O atoms of the phosphate groups) exposed on the surface. When a water molecule is adsorbed on the KDP (101) surface, it can only form a hydrogen bond and an O–K chemical bond with the surface.

The adsorption style (forming an O–K chemical bond and a hydrogen bond with the surface) at positions o and p on the KDP (101) surface (both positions are O–K bridges) is similar to Fig. 7 PDOSs of selected atoms of the water molecule and the (101) surface at position o: (a) atomic orbitals of the H atom of the water molecule and the O atom of the phosphate group and (b) atomic orbitals of the O atom of the water molecule and the K atom of the surface. PDOS of selected atoms of the water molecule and the (101) surface at position p: (c) atomic orbitals of the H atom of the water molecule and the O atom of the phosphate group and (d) atomic orbitals of the O atom of the water molecule and the K atom of the surface. The zero energy is the Fermi level.

Fig. 8 The potential maps of the KDP (100) and (101) surfaces. (a) Represents the KDP (100) surface and (b) represents KDP (101) surface. Red and blue colors mean high potential and low potential, respectively.
that at position h on the KDP (100) surface (P–K bridge). Indeed, position e on the KDP (100) surface (P top site) can be treated as a H–O bridge, as shown in Fig. 8(a). When we locate the most stable positions on the potential maps of the KDP (100) and (101) surfaces, we discover that all these positions are in the valleys between two peaks of high potential. It seems that the parts of high potential (H, O and K atoms exposed on the surface) on the surface pull water molecules to them (in this paper, the pulling effect is between O_W and H_P, O_W and K and H_W and O_P). When the attractions of two states with high surface (eV) is slightly larger (absolute values) than that on the KDP (100) adsorption sites on the KDP (101) surface (–0.57 eV and –0.47 eV). This means that a water molecule can be adsorbed more tightly on the KDP (101) surface than on the KDP (100) surface, indicating that the KDP (101) surface can be more easily dissolved than the (100) surface. Furthermore, the pulling effect of the surface mainly affects the O and H atoms of the water molecule, from which we can deduce that the solute, the phosphate group with an O atom and a H atom exposed, can also be more easily adsorbed on the KDP (101) surface. This might be one reason for the KDP (101) surface growing faster than the (100) surface according to experiments.\textsuperscript{13}

4. Conclusion

In this paper, we studied the adsorption of a single water molecule on the (100) and (101) surfaces of a KDP crystal by DFT calculations for the first time, as far as we know. It was found that the most stable adsorption sites on the KDP (100) surface are the P top site and the P–K bridge site while the most stable sites on the KDP (101) surface are both O–K bridge sites. These positions are at the energy valleys between two states of high potential. The stable configurations are the results of the competition and balance of the pulling effect of two parts of high potential on the surface. We also found the O, H and K atoms on the surfaces are the functional atoms that pull the water molecule toward the surfaces, which we believe is the key to controlling the influences of water adsorption. For example, if we were able to make a new kind of coating that could form strong bonds with these functional atoms, the water molecules in the environment would have few available adsorption sites on the surfaces of the KDP crystal and therefore have little effect on the KDP surfaces. The bond formation between a water molecule and the KDP surfaces is also included in our work. The water molecule can be adsorbed in two different ways—forming two hydrogen bonds with the O and H atoms on the surface or forming a hydrogen bond and an O–K bond with the O and K atoms on the surface. Because the atoms on the surface are ordered, water molecules bonding with these atoms would also show an ordered structure corresponding to the arrangement of these surface atoms. This could partly explain the liquid order at the interface from a theoretical point of view.

Acknowledgements

We are grateful for the support to one of the authors (Yao Liu) from the National Natural Science Foundation of China [grant No. 51402170] and the Fundamental Research Funds of Shandong University [grant No. 2016W1JH40].

References

1. R. C. Miller, D. A. Kleinman and A. Savage, Phys. Rev. Lett., 1963, 11, 146–149.
2. M. J. Chu and S. S. Lee, J. Appl. Phys., 1985, 57, 2647–2649.
3. W. Jamroz and J. Karniewicz, Opt. Quantum Electron., 1979, 11, 23–27.
4. M. Izdebski, W. Kucharczyk and R. E. Raab, J. Opt. Soc. Am. A, 2002, 19, 1417–1421.
5. J. E. Swain, S. E. Stokowski, D. Milam and G. C. Kennedy, Appl. Phys. Lett., 1982, 41, 12–14.
6. J. J. De Yoreo, A. K. Burnham and P. K. Whitman, Int. Mater. Rev., 2002, 47, 113–152.
7. D. Eimerl, Ferroelectrics, 1987, 72, 95–139.
8. N. P. Zaitseva, J. J. De Yoreo, M. R. DeHaven, R. L. Vital, K. E. Montgomery, M. Richardson and L. J. Atherton, J. Cryst. Growth, 1997, 180, 255–262.
9. X. Zhuang, L. Ye, G. Zheng, G. Su, Y. He, X. Lin and Z. Xu, J. Cryst. Growth, 2011, 318, 700–702.
10. M. Nakatsuka, K. Fujioka, T. Kanabe and H. Fujita, J. Cryst. Growth, 1997, 171, 531–537.
11. S. A. De Vries, P. Goedtkindt, S. L. Bennett, W. J. Huisman, M. J. Zwanenburg, D. M. Smilgies, J. J. De Yoreo, W. J. P. Van Enckevort, P. Bennema and E. Vlieg, Phys. Rev. Lett., 1998, 80, 2229.
12. M. Reedijk, J. Arsic, F. Hollander, S. De Vries and E. Vlieg, Phys. Rev. Lett., 2003, 90, 066103.
13. H. Gao, X. Wang, X. Teng and D. Guo, Sci. China: Technol. Sci., 2015, 58, 1877–1883.
14. X. Wang, H. Gao, D. M. Guo, Y. C. Chen and C. P. Song, Adv. Mater. Res., 2013, 797, 423–427.
15. I. M. Thomas, Appl. Opt., 1986, 25, 1481–1483.
16. E. K. Wheeler, R. Fluck, B. Woods and P. K. Whitman, Appl. Opt., 2003, 42, 5545–5550.
17. E. K. Wheeler, P. K. Whitman, T. A. Land, J. De Yoreo, C. B. Thorsness, J. H. McWhirter, M. L. Hanna and E. L. Miller, Appl. Phys. A, 2002, 74, 813–823.
18. A. G. Stack, J. R. Rustad, J. J. DeYoreo, T. A. Land and W. H. Casey, J. Phys. Chem. B, 2004, 108, 18284–18290.
19. D. J. Carter and A. L. Rohl, J. Chem. Theory Comput., 2011, 7, 1604–1609.
20. D. J. Carter, A. L. Rohl and J. D. Gale, J. Chem. Theory Comput., 2006, 2, 797–800.
21. E. V. Stefanovich and T. N. Truong, Chem. Phys. Lett., 1999, 299, 623–629.
22. W. Wang, Y. Shen, X. Wang, Z. Zhou and W. Fei, Appl. Surf. Sci., 2014, 298, 102–108.
23. L. Giordano, J. Goniakowski and J. Suzanne, Phys. Rev. Lett., 1998, 81, 1271–1273.
24. B. Morosin and G. A. Samara, Ferroelectrics, 1972, 3, 49–56.
25 W. Kohn and L. J. Sham, Phys. Rev., 1965, 140, A1133–A1138.
26 M. D. Segall, P. J. D. Lindan, M. J. Probert, C. J. Pickard, P. J. Hasnip, S. J. Clark and M. C. Payne, J. Phys.: Condens. Matter, 2002, 14, 2717–2744.
27 J. P. Perdew, K. Burke and M. Ernzerhof, Phys. Rev. Lett., 1996, 77, 3865–3868.
28 D. Vanderbilt, Phys. Rev. B: Condens. Matter Mater. Phys., 1990, 41, 7892–7895.
29 S. Grimme, J. Comput. Chem., 2006, 27, 1787–1799.
30 D. Y. He, L. J. Qiao, A. A. Volinsky, Y. Bai, M. Wu and W. Y. Chu, Appl. Phys. Lett., 2011, 98, 062905.
31 X. Li, B. Wang, T. Y. Zhang and Y. Su, J. Phys. Chem. C, 2014, 118, 15910–15918.
32 E. Arunan, G. R. Desiraju, R. A. Klein, J. Sadlej, S. Scheiner, I. Alkorta, D. C. Clary, R. H. Crabtree, J. J. Dannenberg and P. Hobza, Pure Appl. Chem., 2011, 83, 1637–1641.
33 N. Zaitseva and L. Carman, Prog. Cryst. Growth Charact. Mater., 2001, 43, 1–118.