I report recent measurements in $b$-hadron decays reconstructed in the full data set of $\sqrt{s} = 1.96$ TeV proton-antiproton collisions collected by the CDF experiment at the Tevatron. These include the final CDF results on: measurements of $CP$ asymmetries in two-body charmless decays of the $B^0$, $B^0_s$, and $\Lambda_b^0$ hadrons; bounds on the $B^0_s$ mixing phase and on the decay width difference of $B^0_s$ mass eigenstates; and updated measurements of branching ratios of $B^0_s \rightarrow J/\psi \phi$ and $B^0_s \rightarrow D_s^{(*)+} D_s^{(*)-}$ decays. All measurements are among the most precise from a single experiment and in agreement with the standard model predictions.
1. Direct $CP$-violation in charmless two-body $b$-hadron decays

Recently, the pattern of direct $CP$ violation in charmless mesonic decays of $B$ mesons has shown some unanticipated discrepancies from expectations that could be accommodated in several simple extensions of the standard model (SM) [1]. However, uncertainties on the contribution of higher-order SM amplitudes has prevented a firm conclusion. Redundant and precise measurements in similar decays related by flavor symmetries provide additional constraints to reduce the theoretical uncertainties and probe non-SM physics in the electro-weak amplitudes. Specifically, measurements of direct $CP$ violation in $B^0 \rightarrow K^- \pi^+$ decays have been proposed as a nearly model-independent test for the presence of non-SM physics [2]. The Cabibbo-Kobayashi-Maskawa (CKM) mechanism predicts a well-defined hierarchy between direct $CP$ violation in $B^0 \rightarrow K^+ \pi^-$ and $B^0 \rightarrow K^- \pi^+$ decays, yielding a significant asymmetry for the latter, of about 30%. Supplementary information could come from $CP$ violation in bottom baryons: $CP$-violating asymmetries in charmless $\Lambda^0_b \rightarrow p \pi^-$ could contribute additional insight.

The displaced vertex trigger of CDF is effective at selecting two-body $b$-hadron decays [3]. We report a recent measurement of $CP$ asymmetries of such decays which uses all of the data from Run II of the Tevatron, corresponding to about $9.3 \, fb^{-1}$ of integrated luminosity [4]. The offline selection is an unbiased and optimized set of requirements inherited from an earlier analysis [5], which relies on a more accurate determination of the same quantities used in the trigger (e.g., two opposite-charged tracks with impact parameter between 0.1 and 1 mm; opening angles between tracks in the range $20^\circ$ and $135^\circ$; $B$ decay length in the transverse plane greater than 0.2 mm) with the addition of two further observables: the isolation of the $B$ candidate and the quality of the three-dimensional fit of the decay point of the $B$ candidate. No more than one $B$ candidate per event is found after the selection, and a mass is assigned to each, using a charged pion mass assignment for both decay products. The resulting $\pi^+ \pi^-$ spectrum is shown in Fig. 1 (left). Backgrounds include mis-reconstructed multibody $b$-hadron decays, causing the shoulder at 5.16 GeV/$c^2$, and random pairs of charged particles. In spite of the 25 MeV/$c^2$ mass resolution of CDF detector for two-body hadronic decays, the various signal modes overlap into an unresolved mass peak near the nominal $B^0$ mass, with a width of about 35 MeV/$c^2$.

We use an unbinned likelihood fit, incorporating kinematic and particle-identification (PID) information, to determine the fraction of each individual signal channel and the charge asymmetries, uncorrected for instrumental effects, of the flavor-specific decays $B^0 \rightarrow K^+ \pi^-$, $B^0 \rightarrow K^- \pi^+$, $\Lambda^0_b \rightarrow p \pi^-$, and $\Lambda^0_b \rightarrow p K^-$. The decay flavor is inferred from the charges of final state particles assuming equal numbers of $b$ and $\bar{b}$ quarks at production. Any effect from $CP$ violation in $B$-meson flavor mixing is assumed to be negligible. The likelihood exploits the kinematic differences among the decay modes, enhancing statistical separation power between $\pi \pi$ and $KK$ (or $K \pi$) final states. The kinematic information is summarized by three loosely correlated variables: the square of the invariant mass $m^2_{\pi\pi}$; the signed momentum imbalance $\beta = (p^+ - p^-)/(p^+ + p^-)$, where $p^+$ ($p^-$) is the the momentum of the positive (negative) particle; and the scalar sum of particle momenta $p = p^+ + p^-$. Kinematic fit templates are extracted from simulation for signal and physics background, while they are extracted from an independent sample for combinatorial background. Mass line shapes are accurately described for the non-Gaussian resolution tails and for the effects of the final state radiation of soft photons. This resolution model was checked against the observed shape.
of the 3.8 million $D^0 \rightarrow K^-\pi^+$ decays in a sample of $D^{++} \rightarrow D^0\pi^+$ decays collected with a similar trigger selection. This sample was also used to calibrate the PID through the measurement of the specific ionization energy-loss ($dE/dx$) of kaons and pions in the drift chamber, using the charge of the $D^{++}$ pion to identify the $D^0$ decay products. The $dE/dx$ response of protons was determined from a sample of about 0.3 million $\Lambda \rightarrow p\pi^-$ decays, where the kinematics and the momentum threshold of the trigger allow unambiguous identification of the decay products. The statistical separation between kaons and pions is about 1.4$\sigma$, while the ionization rates of protons and kaons are quite similar in the momentum range of interest. The signal yields from the fit are corrected for different detection efficiencies extracted from control samples in data to determine the physical asymmetries. Simulation is used only to account for small differences between the kinematics of decays and control signals. The corrections for decays into the $K^+\pi^-$ final state are extracted from a sample of about 30 million untagged $D^0 \rightarrow K^-\pi^+$ decays. For the $\Lambda_b^0 \rightarrow p\pi^-$ asymmetry, the factor is derived from a control sample of $\Lambda \rightarrow p\pi$ decays. The $pK^-$ factor is extracted by combining the previous ones and assuming the trigger and reconstruction efficiency for two particles factorizes as the product of the single-particle efficiencies.

The final results are listed in Tab. 1. The asymmetry $\mathcal{A}_{CP}(B^0 \rightarrow K^+\pi^-)$ is consistent with results from $B$-factories and LHCb. The measured $\mathcal{A}_{CP}(B_s^0 \rightarrow K^-\pi^+)$ confirms the LHCb evidence with the same level of resolution. Systematic uncertainties on such asymmetries are largely due to variation of the fit results against different templates for combinatorial background, signal mass distributions and PID modeling. The observed asymmetries of the $\Lambda_b^0$ decays are consistent with zero. Their systematic uncertainty is dominated by the variation of unknown polarization amplitudes in the templates. They are in agreement with the previous results from CDF and supersede them [5].

2. Measurement of the $B_s^0 \rightarrow J/\psi\phi$ time-evolution and branching ratio in the complete CDF dataset

The $B_s^0 \rightarrow J/\psi\phi$ mixing is a promising process for searches for new physics (NP), given the D0 3.9$\sigma$ anomaly in dimuon charge asymmetry [6]. If the anomaly is due to new dynamics in the $B_s^0$ sector the phase difference between the $B_s^0 \rightarrow B_s^0$ mixing amplitude and the amplitude of $B_s^0$ and $\bar{B}_s^0$ decays into common final states, $\phi_s$, would be significantly altered with respect to its nearly vanishing value expected in the SM. A non-CKM enhancement of $\phi_s$ can also decrease the decay width difference $\Delta \Gamma$, between the heavy and light mass-eigenstates of the $B_s^0$ meson. The analysis of the time evolution of $B_s^0 \rightarrow J/\psi\phi$ decays is the most effective experimental probe of such a CP-violating phase. Since the decay is dominated by a single real amplitude, the phase difference equals the mixing phase to a good approximation. Early Tevatron measurements have shown a mild discrepancy of about 2$\sigma$ with the SM expectation [7]. Latest updates by CDF and D0 are in better agreement with the SM, as well as measurements provided by LHCb [8, 9, 10, 11].

Here we report the new CDF update using the complete dataset of 9.6 fb$^{-1}$ which comprises about 11 000 $B_s^0 \rightarrow J/\psi\phi$ decays collected by the dimuon trigger [12]. The decays are fully reconstructed through four tracks that fit to a common decay point separated from the beam line, two matched to muon pairs consistent with a $J/\psi$ decay, and two consistent with a $\phi \rightarrow K^+K^-$ decay. A joint fit that exploits the candidate-specific information given by the $B$ mass, decay time and production flavor, along with the decay angles of kaons and muons, is used to determine both $\phi_s$. 

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and $\Delta \Gamma_s$. The analysis closely follows the previous determination obtained on a subset of the data [8]. The only major difference is the use of an updated calibration of the tagging algorithm that uses information from the decay of the opposite side bottom hadron in the event to determine the flavor of the $B^0_s$ at its production, with tagging power $(1.39 \pm 0.05)\%$. The information from the tagger that exploits charge-flavor correlations of the neighboring kaon to the $B^0_s$ is instead restricted to only half of the sample, in which has tagging power $(3.5 \pm 1.4)\%$, because its calibration is feasible for early data only. This degrades the statistical resolution on $\phi_s$ by no more than 15%. A decay-time resolution of $\sim 90$ fs allows resolving the fast $B^0_s$ oscillations to increase sensitivity on the mixing phase.

Included in the analysis is also the $CP$-odd $s$-wave component which originates from the non-resonant $K^+K^-$ pair or from $f_0(980)$ decays. The fraction of $s$-wave in the $K^+K^-$ mass range 1.009–1.028 GeV/$c^2$ is determined from the angular information to be consistent with zero with $\sigma(2\%)$ uncertainty, which is in agreement with our previous determination [8] and the LHCb [10] and ATLAS results [11], and inconsistent with the D0 determination [9]. An auxiliary simultaneous fit of the $J/\psi K^+K^-$ and $K^+K^-$ mass distributions, which includes for the first time the full resonance structure of the $B^0\to J/\psi K^+\pi^-$, determines a $(0.8 \pm 0.2(stat))\%$ $K^+K^-$ $s$-wave contribution, in agreement with the central fit. The contamination from mis-identified $B^0$ decays is $(8.0 \pm 0.2(stat))\%$, which is significantly larger than the 2% values derived assuming only $P$-wave $B^0$ decays [8]. If neglected, this additional $B^0$ component could mimic a larger $K^+K^-$ $s$-wave than is present.

The 68% and 95% confidence regions in the plane $(\phi_s, \Delta \Gamma_s)$ obtained using a profile-likelihood ratio ordering with frequentist inclusion of systematic uncertainties are reported in Fig. 1 (right). The confidence interval for the mixing phase is $\phi_s \in [-0.60, 0.12]$ rad at 68% C.L., in agreement with the CKM value and other recent determinations [9, 10, 11]. This is the final CDF measurement on the $B^0_s$ mixing phase, and provides a factor 40% improvement in resolution with respect to the latest determination. In Tab. 1, we also report the measurements of $\Delta \Gamma_s$ and of the $B^0_s$ lifetime $\tau_s$, under the hypothesis of a SM value for $\phi_s$, which are in agreement with other experiments’ results [9, 10, 11].

The Run II dimuon data set is also exploited for measuring the ratio of the $B^0_s\to J/\psi \phi$ and $B^0\to J/\psi K^*(892)^0$ branching fractions, $R = (f_s/f_d)(\mathcal{B}(B^0_s\to J/\psi \phi)/\mathcal{B}(B^0\to J/\psi K^*(892)^0))$, where $f_{s(d)}$ is the fragmentation fraction of the $s(d)$ quark [13]. We adopt an offline selection that differs from the selection for the $\phi$ measurement since it is optimized toward the measurement of $R$. We extract the $B^0_s$ and $B^0$ yields through a fit to the binned $J/\psi K^+K^-$ and $J/\psi K^+\pi^-$ invariant mass distributions. After application of a relative acceptance factor determined from simulation, we measure $R = 0.239 \pm 0.003(stat) \pm 0.019(syst)$. Systematic uncertainties are dominated by the modeling of the background and signal templates in the fit and by the variation within uncertainties of the world average value of $B$ lifetimes and polarization amplitudes in the simulation for the acceptance’s estimation. Using the most recent CDF measurement [14] of $f_s/(f_s + f_d)\mathcal{B}(D_s\to \phi \pi)$ combined with the PDG value of $\mathcal{B}(D_s\to \phi \pi)$ [15] to extract $(f_s/f_d)$ and the PDG value of $\mathcal{B}(B^0\to J/\psi K^*(892)^0)$ [15], we find the branching ratio $\mathcal{B}(B^0_s\to J/\psi \phi)$ reported in Tab. 1, in agreement with and with similar resolution to Belle’s latest result [16]. Using the latter, we also compute the ratio $f_s/f_d$ (Tab. 1). The analysis is also performed in bins of $B^0_s$ transverse momentum in a range of $6 < p_T < 27$ GeV/$c$, showing no dependence of $f_s/f_d$ versus $p_T$. 

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3. Measurement of $B_{s}^{0} \rightarrow D_{s}^{(*)+} D_{s}^{(*)-}$ branching ratios

A measurement of $B_{s}^{0}$ production rate times the $B_{s}^{0} \rightarrow D_{s}^{(*)+} D_{s}^{(*)-}$ branching ratio relative to the normalization mode $B^{0} \rightarrow D_{s}^{+} D^{-}$ is performed using a data sample corresponding to an integrated luminosity of 6.8 fb$^{-1}$ recorded by the displaced track trigger [17]. The decays $D_{s}^{+} \rightarrow K^{+} K^{-} \pi^{+}$ and $D^{-} \rightarrow K^{-} \pi^{+} \pi^{+}$ are reconstructed from combinations of three tracks with appropriate charge and mass hypothesis assignments, fitted to a common vertex and then combined into another vertex to form $B_{s}^{0}$ candidates. For the first time in this channel, the Dalitz structure of the intermediate states is exploited for an accurate evaluation of acceptances and efficiencies. The relative branching fractions are determined in a simultaneous maximum likelihood fit to mass distributions of two signal samples, $(\phi \pi^{+}) (\phi \pi^{-})$ and $(K^{*}(892)^{0} K^{+}) (\phi \pi^{-})$, and two normalization samples, $(\phi \pi^{+}) (K^{+} \pi^{-} \pi^{-})$ and $(K^{*}(892)^{0} K^{+}) (K^{+} \pi^{-} \pi^{-})$. Using measured values of production and relative branching fractions, the absolute branching fractions shown in Tab. 1 are derived. These results are the most precise to date from a single experiment and can provide information on the decay width difference $\Delta \Gamma_{s}$.

4. Conclusions

I have reported recent measurements in $b$-hadron decays which exploit the full CDF data set. The measured $CP$ asymmetry of $B_{s}^{0} \rightarrow K^{-} \pi^{+}$ decays confirms the LHCb result with similar resolution, providing strong evidence of direct $CP$ violation in this decay mode. Unique measurements of $CP$ asymmetries in $\Lambda_{c}^{0}$ decays are also presented. In the $B_{s}^{0} - \bar{B}_{s}^{0}$ mixing sector, tensions with SM predictions are now softened by latest updates of $\phi_{s}$ and $\Delta \Gamma_{s}$ bounds. From the large data set collected, we also gain a more precise measurement of the $B_{s}^{0} \rightarrow J/\psi \phi$ branching ratio and investigation of dependences of the fragmentation fraction $f_{s}/f_{D}$ on the $B$ transverse momentum. Finally, we obtain the world’s best measurement of $B_{s}^{0} \rightarrow D_{s}^{(*)+} D_{s}^{(*)-}$ branching ratios to date. Analyses of the unique ($\phi \bar{p}$ charge-symmetric) and well-understood (10-years expertise) data sample acquired by CDF are still in progress and may provide interesting results in the near future.
Table 1: Summary of results of the measurements described in this report.

| Measurement | Result |
|-------------|--------|
| $\phi_s$ | $(-8.3 \pm 1.3 \text{(stat)} \pm 0.3 \text{(syst)})\%$ |
| $\Delta \Gamma_s$ | $0.068 \pm 0.026 \text{(stat)} \pm 0.009 \text{(syst)} \text{ ps}^{-1}$ |
| $\tau_s$ | $1.528 \pm 0.019 \text{(stat)} \pm 0.009 \text{(syst)} \text{ ps}$ |
| $\phi(\Upsilon)$ | $(0.118 \pm 0.002 \text{(stat)} \pm 0.009 \text{(syst)} \pm 0.015 \text{(BR)})\%$ |
| $f_s/f_d$ | $0.254 \pm 0.003 \text{(stat)} \pm 0.020 \text{(syst)} \pm 0.044 \text{(BR)}$ |
| $\phi(\B_s^0 \rightarrow J/\psi \phi)$ | $(0.49 \pm 0.06 \text{(stat)} \pm 0.05 \text{(syst)} \pm 0.08 \text{(BR)})\%$ |
| $\Delta \Gamma(\B_s^0 \rightarrow J/\psi \phi)$ | $(1.13 \pm 0.12 \text{(stat)} \pm 0.09 \text{(syst)} \pm 0.19 \text{(BR)})\%$ |
| $\phi(\B_s^0 \rightarrow D_s^\pm D_s^\mp)$ | $(1.75 \pm 0.19 \text{(stat)} \pm 0.17 \text{(syst)} \pm 0.29 \text{(BR)})\%$ |
| $\phi(\B_s^0 \rightarrow D_s^{(*) \pm} D_s^\mp)$ | $(3.38 \pm 0.25 \text{(stat)} \pm 0.30 \text{(syst)} \pm 0.56 \text{(BR)})\%$ |

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