Post-main-sequence debris from rotation-induced YORP break-up of small bodies II: multiple fissions, internal strengths and binary production

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ABSTRACT

Over one quarter of white dwarfs contain observable metallic debris from the breakup of exo-asteroids. Understanding the physical and orbital history of this debris would enable us to self-consistently link planetary system formation and fate. One major debris reservoir is generated by YORP-induced rotational fission during the giant branch phases of stellar evolution, where the stellar luminosity can exceed the Sun’s by four orders of magnitude. Here, we determine the efficacy of the giant branch YORP effect for asteroids with nonzero internal strength, and model post-fission evolution by imposing simple analytic fragmentation prescriptions. We find that even the highest realistic internal strengths cannot prevent the widespread fragmentation of asteroids and the production of a debris field over 100 au in size. We compute the number of successive fission events as they occur in progressively smaller time intervals as the star ascends the giant branches, providing a way to generate size distributions of asteroid fragments. The results are highly insensitive to progenitor stellar mass. We also conclude that the ease with which giant branch YORP breakup can generate binary asteroid subsystems is strongly dependent on internal strength. Formed binary subsystems in turn could be short-lived due to the resulting luminosity-enhanced BYORP effect.

Key words: Kuiper belt: general minor planets, asteroids: general planets and satellites: dynamical evolution and stability stars: AGB and post-AGB stars: evolution white dwarfs.

1 INTRODUCTION

Understanding the full lifecycle of planetary systems requires connecting their formation around main sequence stars with their fate around white dwarfs. The glue that binds these two endpoints are giant branch stars, which arguably produce the most violent changes to the system evolution. Such violence is appropriately showcased by how intact planets dominate observations of main-sequence exoplanetary systems whereas shattered asteroidal debris dominate observations of white dwarf exo-planetary systems.

Asteroids are hence a key component of our understanding. White dwarfs represent stars which are both dense enough to stratify all infalling material into its constituent atoms (Schatzman 1958) and differentiated enough to feature a photosphere consisting of entirely hydrogen and/or helium. Consequently, observations of infalling material are unambiguous and direct, and represent the most substantial available windows into the bulk chemical composition of exo-planetary material. Between one-quarter and one-half of white dwarfs feature rocky debris (Zuckerman et al. 2003, 2014; Koester et al. 2014) and 20 different metals have now been observed in these remnants (e.g. Gänscic et al. 2012; Jura & Young 2014; Melis & Dufour 2017; Xu et al. 2017; Harrison et al. 2018; Hollands et al. 2018; Doyle et al. 2019; Swan et al. 2019).

Asteroids are also showcased in these systems in other respects. Minor planets have been observed orbiting the white dwarfs WD 1145+017 (Vanderburg et al. 2013) and SDSS J1228+1040 (Manser et al. 2019) in real time and might generate the transit dips seen in ZTF J0139+5245.

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(Vanderbosch et al. 2019). Asteroids are also the most likely progenitors for the over 40 known white dwarf discs (e.g. Zuckerman & Becklin 1987; Gänscicke et al. 2006; Farhi 2011; Dennihy et al. 2018). In fact, the minor planet orbiting SDSS J1228+1040 is embedded within the debris disc, and resides well within the star’s Roche radius, suggesting that the asteroid has high internal strength (Veras et al. 2017). That object is probably better characterised as an asteroid-sized ferrous planetary core fragment, which also has not been observed in main-sequence systems.

The dynamical pathways leading to asteroidal signatures in white dwarf planetary systems remain a subject of debate and suffer from a dearth of dedicated studies (Veras 2016a). Although these pathways are first shaped during planet formation and subsequent main-sequence evolution, during the giant branch phase the system is transformed in three major ways:

- **Stellar mass loss.** A giant branch star will lose between about one-half and three-quarters of its mass non-constant with time. For Solar-mass stars, most mass is lost at the tips of the red giant branch and asymptotic giant branch phases; for more massive stars, the red giant branch phase is effectively suppressed. In general, stellar mass loss changes all of the orbital elements of surrounding material (Veras et al. 2013a; Dasopoulos & Kalogera 2016a,b). However, imposition of the reasonable assumption of isotropy for the mass loss results in simplified orbital changes, when the only variations are in the semimajor axis, eccentricity, and argument of pericentre (Omari et al. 1992; Hadilemmetria 1963). A further simplification occurs when considering orbital changes within about several hundred au: here the so-called adiabatic approximation can be employed (Veras et al. 2011), such that (effectively) only the semimajor axis changes, and at a rate proportional to the mass loss. Consequently, unless one considers the effect of mass loss on Oort clouds (Alcock et al. 1986; Parrott & Alcock 1993; Veras & Wyatt 2012; Veras et al. 2014a; Stone et al. 2017; Caiazzo & Heyl 2017), most planets and asteroids will simply increase their semimajor axes by a factor of 2-4 due to giant branch mass loss.

- **Stellar radius expansion** Upon ascending the giant branches, stars will increase their radii by a factor of hundreds; in the solar system, at least Mercury and Venus will be swallowed (Schroder & Smith 2008; Veras 2016a). The resulting tidal interaction with planets is significant and have been well-studied (Villaver & Livio 2007; Kunitomo et al. 2011; Mustill & Villaver 2012; Adams & Bloch 2013; Nordhaus & Spiegel 2013; Villaver et al. 2014; Madappatt et al. 2016; Staff et al. 2014; Gallet et al. 2017; Rao et al. 2018; Sun et al. 2018). In contrast, giant branch tidal effects on asteroids have not been studied in any appreciable way, although asteroids are small enough to not extend the critical tidal engulfment distance beyond the stellar surface.

- **Stellar luminosity enhancement** The greatest danger to asteroids is stellar radiation. Stars at the tip of the asymptotic giant branch are tens of thousands of times more luminous than the sun. The consequences for planetary atmospheres and surfaces remain largely unexplored (Schreiber et al. 2019), but should not alter their orbits and spins. However, the same is not true for asteroids. Asteroids are easily flung about (Veras et al. 2015a, 2016a) due to a radiative effect known as the Yarkovsky effect (Radzievskii 1954; Peterson 1974). Asteroids can also easily be spun up to breakup speed (Veras et al. 2014c) (hereafter Paper I) through another radiative effect known as the YORP effect (Rubincam 2000). The result is both an orbital rearrangement and a debris field spreading out to hundreds of au.

These asteroids and this debris are then later propelled towards the white dwarf through a combination of Poynting-Robertson drag (Stone et al. 2013; Veras et al. 2015a) and gravitational interactions with planets (Bonsor & Veras 2013; Debels et al. 2013; Frewer & Hansen 2014; Veras et al. 2016; Antoniadou & Veras 2016, 2019; Mustill et al. 2018; Smallwood et al. 2018) or moons (Payne et al. 2016; 2017) or binary stellar companions (Bonsor & Veras 2013; Hamers & Portegies Zwart 2016; Petrovich & Munoz 2017; Stephan, Naoz & Zuckerman 2017; Stephan et al. 2018). These substellar bodies may then break up en route towards the white dwarf (Makarov & Veras 2014) or within its Roche radius, forming a debris disc (Graham et al. 1990; Jura 2003; Debels et al. 2012; Bear & Soker 2013; Veras et al. 2014b; Malamud & Perets 2020a,b) or becoming embedded in an existing disc (Grishin & Veras 2019).

Hence, an understanding of the distribution and type of debris in giant branch systems crucially allows one to link them with observations of planetary debris in white dwarf planetary systems. The need for this understanding will become more urgent with discoveries of major planets orbiting white dwarfs (Gänscicke et al. 2019) and the expected order-of-magnitude increase of debris-rich systems due to the entire known population of white dwarfs increasing by a factor of 8 in the year 2018 (Gentile Fusillo et al. 2019).

Despite this urgency, the only paper which has so-far addressed giant branch YORP break-up of asteroids is Paper I. That paper introduced the concept of ubiquitous destruction due to giant-branch YORP effects, but modelled the process with the most basic assumptions: with no internal strength nor fragmentation prescription. This paper aims to generalise Paper I by incorporating these two features, a task which is facilitated by the recent investigation of Scheeres (2018). Our paper does not merge the YORP and Yarkovsky effects in a self-consistent framework, which even for the simplest YORP formalism would be beyond the scope of this study (Veras et al. 2015a). Our paper also does not strive to achieve the level of fine detail often required to model the solar system YORP effect with features like local topography and avalanches (e.g. Gohhov & Kruegh 2012; Statler et al. 2014; Yu et al. 2018).

We aim instead to provide useful order-of-magnitude values which can be used in future studies. In Section 2 we perform our analysis. We discuss our results in Section 3 and conclude in Section 4.

## 2 Asteroid Evolution due to YORP

### 2.1 Spin-up

We begin by quantifying the extent to which an asteroid spins up over time due to giant branch luminosity. We can express this evolution from Scheeres (2007) and Paper I, but in a similar form to equation 1 of Scheeres (2018), as
Here ω is the asteroid’s spin rate, $R_0$ its initial radius, $a(t)$ its semimajor axis, ρ its density (taken to be 2 g/cm$^3$ throughout the paper) and e its eccentricity (taken to be 0 throughout the paper). The luminosity of the star is $L_*(t)$ and the solar radiation constant $\Phi$ is taken to be 1 $\times 10^{17}$ kg m/s$^2$. The constant $C$ expresses the amount of asymmetry and obliquity in the asteroid; following [Scheeres 2018], we adopt the two values $C = 10^{-2}$ and $C = 10^{-3}$ as bounds on the shape.

Time dependencies are explicitly stated for spin, luminosity and semimajor axis, because these are the only three values which we assume change continuously with time. The asteroid’s eccentricity remains fixed because we employ the adiabatic approximation for mass loss ([Veras et al. 2011]) as the semimajor axes we will be considering are all under about 600 au.

When the asteroid undergoes fission, we will replace $R_0$ with a fissioned component. Otherwise, $R_0$ remains fixed. In reality, $R_0$ could change continuously in time due to sublimation, particularly if the asteroid contains an internal reservoir of volatiles ([Jura & Xu 2010, 2012; Farihi et al. 2013; Raddi et al. 2013; Malamud & Perets 2014; Gentile Fusillo et al. 2013; Malamud & Perets 2017a, b]). Orbital changes could result from anisotropic out-gassing ([Marsden et al. 1973; Froeschle & Rickman 1986; Królikowska 2004; Steckloff & Jacobson 2014; Veras et al. 2015a]) whereas spin changes could directly result from equation (1) due to a reduction of $R_0$.

Integration of equation (1) requires a value for the initial asteroid spin, a stellar evolution profile, and an integration duration. To simplify our analysis and reduce the phase space to explore, we model only spin increases and adopt two choices for $\omega(0)$. The first is $\omega(0) = 0$ rad/s, and the second is $\omega(0) = -\sqrt{4 \pi G \rho / 3}$. This latter choice is the negative value of the breakup spin rate for a strengthless rubble pile ([Scheeres 2018]), and hence would require the greatest injection of positive spin to break apart. The stellar evolution profiles are taken from the SSE code ([Hurley et al. 2000]). These profiles include a Reiners mass loss prescription ([Reiners 1973, 1977]) along the red giant branch phase and a superwind prescription along the asymptotic giant branch phase ([Vassiliadis & Wood 1993]) with the default values (including Solar metallicity) given within SSE. We integrate for the entire red giant and asymptotic giant branch phases, and then for 1 Gyr of white dwarf cooling. Doing so allows us to confirm that white dwarf radiation has little effect on asteroids whose orbits have already been pushed outward by a factor of a few.

One helpful finding is that the interplay between $a(t)$, $L_*(t)$ and the duration of the giant branch phases produces results which are independent of stellar mass in an order-of-magnitude manner, removing that variable from further consideration. To demonstrate this effect, in Fig. 1 we plot the final asteroid spin for three different initial sets of parameters, after each was integrated separately around 31 different main-sequence stellar masses ranging from 1.0 $M_\odot$ to 3.0 $M_\odot$.2 These parameter sets straddle extremes (Set 1: $a(0) = 3$ au and $R_0 = 100$ m; Set 2: $a(0) = 10$ au and $R_0 = 1$ km; Set 3: $a(0) = 100$ au and $R_0 = 10$ km) and all assume $C = 10^{-3}$. We note that in the first two of these cases, the asteroids would have probably broken apart long before these final spins were achieved: this plot is just for demonstration purposes, to help show the invariance of the results with respect to stellar mass.

We henceforth assume a main-sequence progenitor mass of 2.0 $M_\odot$ throughout the remainder of the paper.

### 2.2 Internal strength

We now compute how strong a rubble-pile asteroid must be to resist giant branch YORP break-up. By “asteroid strength” we refer to the strength of the bonds between the rubble components (e.g. between different boulders and grains), which is usually less than 1 kPa ([Table 3 of Scheeres 2018]). The individual boulders and grains themselves have much different and higher internal strengths, usually greater than 1 MPa ([Tables 1-2 of Scheeres et al. 2013]). We will discuss this dichotomy and the implications further in Section 3. For the remainder of Section 2, however, we will assume that each successive fission produces fragments which are larger than the constituent boulders and grains.

The failure spin rate $\omega_{\text{fail}}$ of an asteroid can be approximated as ([Sánchez & Scheeres 2014; Steckloff & Jacobson 2014; Scheeres 2018])

$$\omega_{\text{fail}}^2 \approx \frac{4 \pi G \rho}{3} + \frac{2 \sigma}{\rho R_0} \left( \frac{2}{3} \right),$$

where $\sigma$ is its tensile, uniaxial strength. The fraction of (2/3)

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2 This range bounds the progenitor masses for the vast majority of known white dwarf planetary systems ([Tremblay et al. 2010]).
in the rightmost term is a value arising from a representative angle of friction. By equating the final spin state of an asteroid $\omega_{\text{final}}$ with $\omega_{\text{crit}}$, we then obtain the critical tensile strength $\sigma_{\text{crit}}$ which is the minimum that the asteroid would need to harbour in order to survive post-main-sequence evolution:

$$\sigma_{\text{crit}} = \frac{1}{4} R_0^2 \rho (3 \omega_{\text{final}}^2 - 4 \pi G \rho).$$ (3)

We compute $\sigma_{\text{crit}}$ for a range of asteroid semimajor axis and radii in Fig. 2. On each plot, we performed 72 integrations (for eight different $a(0)$ values and nine different $R_0$ values). The right endpoint of each curve indicates the largest asteroid which experienced fission; larger asteroids, which do not undergo fission, need not have any internal strength. Note that survival occurs only for the largest asteroids at the furthest distances from the star.

For the asteroids which do undergo fission, in almost every case, $\sigma_{\text{crit}}$ is unrealistically high (see, for example, Table 3 of Scheeres 2018 and, for meteorite strengths, Table 1 of Scheeres et al. 2014). Hence, the inclusion of internal strength does not change the results of Paper I. The only cases where a realistic internal strength can prevent breakup are for $a(0) \gtrsim 50$ au and $R_0 \lesssim 0.5$ km.

### 2.3 Fragmentation

Having established the robustness of the destructive giant branch YORP process, we now investigate post-fission evolution, which was not quantified in Paper I. Scheeres 2018 provided a straightforward fragmentation prescription that is well-suited for our purposes. He assumed that the asteroid will split into $N$ equal bodies of radii

$$R_1 = N^{-1/3} R_0,$$ (4)

such that mass is conserved and after the ith fission, there will be a total of $N^i$ bodies, each with radii

$$R_i = N^{-i/3} R_0.$$ (5)

The reduction of asteroid radius due to a fission increases its spin rate of spin acceleration (equation 1) and, if the asteroid contains internal strength, the failure spin rate (equation 2). The asteroid spin rate increase is steeper than the failure spin rate increase. Combined with the steep increase in stellar luminosity, particularly along the tip of the asymptotic giant branch phase, the result can be a relentless fission cascade. This cascade would cease – or at least our fragmentation model would no longer be applicable – at a value of $R_i$ corresponding to the constituents of the asteroid (boulders or grains).

The realistic maximum number of fissions depends largely on the chosen value of $N$. For example, $N = 2$ and $i = 10$ reduces a 10 km asteroid into about $10^3$ separate 1 km asteroids, whereas $N = 5$ and $i = 10$ reduces a 10 km asteroid into about $10^7$ separate 50 m asteroids.

How the spins of the child asteroids are reset after a fission significantly affects the subsequent number of fissions, but depends on details of the disruption dynamics that we do not model here. One reasonable possibility is that the post-fission spin rate is equal to the previous fission spin rate. We consider two other extreme cases, one where the child asteroid spins reset to zero, and the other where their spin rates are reversed to the rubble pile limit ($-\sqrt{4\pi G \rho / 3}$).

In order to demonstrate a typical asteroid evolution with this fragmentation model, we have plotted spin rate versus time for a $R_0 = 4.25$ km with high internal strength ($\sigma = 10^3$ Pa) in Fig. 3. In this plot, we assume that the post-fission spin rate resets to zero, and $N = 6$. The parent asteroid undergoes four fissions, ultimately producing about 1300 child asteroids, with successive radii of $R_1 = 2.3$ km, $R_2 = 1.3$ km, $R_3 = 0.7$ km and $R_4 = 0.39$ km. The locations of the fissions are indicated by black dots, and their increase (due to a large finite strength of $\sigma = 1000$ Pa combined with asteroid radius reduction; see equation 2) is tracked with the black dashed lines. The last horizontal black dashed segment is never reached.

In the figure, all of the fissions occur within 3 Myr. This brief destructive epoch occurs at the tip of the asymptotic giant branch phase (for a 2.0$M_\odot$ progenitor star). The time to each subsequent fission becomes progressively shorter. The rate of increase of the spin rate of the last child generation is reduced to a negligible value abruptly as the star becomes a white dwarf. The white dwarf’s rapid luminosity decrease (e.g. Althaus et al. 2009) combined with the expanded orbit of the child asteroids effectively flattlines their spin rate curves.

We next determine the number of fissions experienced for different types and locations of asteroids. We report the results in a series of 7 plots in Figs. 4-11. All plots illustrate the number of fissions versus initial asteroid radius, for $C = 10^{-3}$. The entire range of asteroid radii which were used in the integrations is shown; an absence of a dot indicates that the number of fissions for that integration was greater than 10. A value of 0 fissions indicate that the asteroid survived giant branch YORP spin-up. One common characteristic of all plots is that there exists only a narrow range of radii for which the number of fissions is between 0 and 10.

In the first two figures (figure 4-5), we consider asteroids with $a(0) = 5$ au. The only difference between these two figures is how the spin is reset after each fission (to 0 in the first figure, and to the negative cohesionless limit in the second). This difference changes the critical radii at which fission occurs by 1-2 km, and has a much stronger dependence than the inclusion of internal strength (right panels).

In the next figure (figure 6), we consider asteroids with $a(0) = 30$ au. Consequently, the asteroid radii ($x$-axes) for which the number of fissions lies between 0 and 10 is lowered by an order of magnitude from figures 4-5. Also, the difference in the two plots in figure 6 demonstrates that the inclusion of internal strength has a stronger relative effect than in figures 4-5.

The final figure (figure 7) illustrates a $a(0) = 200$ au case, which might be considered extreme in main-sequence systems, but not here. The plot illustrates that asteroids with radii on the order of 100 m will regularly undergo fissions and hence produce debris in those regions of white dwarf planetary systems.

### 2.4 Forming binary asteroids

A fission can produce bound components in some circumstances, forming (in the case of 2 or 3 child asteroids) a “bi-
Figure 2. The critical (or minimum) internal strength an asteroid would need in order to survive giant branch YORP spin-up for $a(0)$ values ranging from 3 au (top curves) to 100 au (bottom curves). The left and right plots illustrate the shape- and obliquity-based bounding cases corresponding to $C = 10^{-3}$ and $C = 10^{-2}$. A uniform grid of 72 integrations was performed on each plot in $R_0-a(0)$ space: each dot represents an integration for an asteroid that would be destroyed without any internal strength, and the rightmost dot on each curve represents the largest asteroid that is destroyed for a given $a(0)$. The plots demonstrate that asteroids require unrealistically high values of internal strength to survive rotational fission.

Successive asteroid fissions for $R_0 = 4.25$ km, $a_0 = 5$ au,

$\sigma = 1000$ Pa, $N = 6$, $\omega$ reset to 0 rad/s at each fission

Figure 3. Spin evolution of a $R_0 = 4.25$ km asteroid which undergoes four fissions during giant branch evolution. In each fission, the progenitor splits into 6 equal child asteroids, generating a total of about 1300 asteroids of radii $R_4 = 0.39$ km. Because the asteroids have internal strength ($\sigma = 10^3$ Pa), the failure spin rate increases with each fission. The star becomes a white dwarf soon after the last fission, effectively halting any further spin rate increases.
Figure 4. Number of fissions for $a(0) = 5$ au asteroids, both without strength (left panel) and with high strength (right panel). After each fission, the spin rate is reset to stationary. In both plots, the curves from left to right correspond to an increasing number of fissions from 2 to 125.

Figure 5. Same as Fig. 4 except here after each fission the spin rate is reversed and set to the extreme value of the cohesionless limit.

Figure 6. Number of fissions for $a(0) = 30$ au asteroids, both without strength (left panel) and with high strength (right panel).
A binary asteroid or "ternary asteroid". Achieving this state requires the subsystem to attain net positive energy.

Scheeres (2018) provided a criterion for escape for \( N = 2 \), which requires the child asteroids to be unequal in radii and mass (unlike in the last subsection). Now assume that the two children have radii \( R_{1a} \) and \( R_{1b} \). Further assume \( R_{1a} > R_{1b} \) such that

\[
R_{1a} = k_1 R_{1b}
\]

with \( k_1 > 1 \). Then the parent and child radii are related through

\[
R_0 = \left( R_{1a}^3 + R_{1b}^3 \right)^{1/3},
\]

\[
R_{1a} = \frac{R_0 k_1}{(k_1^3 + 1)^{1/3}},
\]

\[
R_{1b} = \frac{R_0}{(k_1^3 + 1)^{1/3}}.
\]

The critical spin rate below which these two children would remain bound to each other as a binary asteroid (Scheeres 2018) can be written as

\[
\omega_{\text{bound}} = \frac{8\pi G \rho}{3} \frac{R_{1a}^3 + R_{1b}^3}{(R_{1a} + R_{1b})^3} = \frac{8\pi G \rho}{3} \left( 1 + k_1^3 \right),
\]

\[
\omega_{\text{bound}} = \frac{8\pi G \rho}{3} \frac{R_{1a}^3 + R_{1b}^3}{(R_{1a} + R_{1b})^3} = \frac{8\pi G \rho}{3} \left( 1 + k_1^3 \right).
\]

The minimum value of \( k_1 \) for which the fissioned binary would remain bound (\( k_{1\text{,min}} \)) is then given through \( \omega_{\text{bound}} = \omega_{\text{fiss}} \), yielding

\[
\frac{1 + k_1^{3\text{,min}}}{(1 + k_{1\text{,min}})^3} = \frac{1}{2} + \frac{\sigma}{2G\rho R_0^2}.
\]

Solving for \( k_{1\text{,min}} \) gives

\[
k_{1\text{,min}} = \frac{\sigma + 2\pi G R_0^2 \rho^2 + GR_0 \rho \sqrt{3\pi (\pi R_0^2 \rho^2 + 2\rho)}}{\pi G R_0^2 \rho^2 - \sigma}.
\]

Hence, in order for a binary to remain bound, both \( k_1 \geq 2 + \sqrt{3} \approx 3.73 \) (the strengthless limit) and \( R_0 > \sqrt{\sigma/(\pi G \rho^2)} \).

Consequently, a strengthless parent asteroid of any size can break apart into two bound components. For an asteroid with nonzero internal strength, the minimum parent radius that could produce a binary asteroid is 110 m, 350 m and 1.1 km for respectively \( \sigma = 10, 10^2, 10^3 \) Pa. For these asteroids, we plot \( k_{1\text{,min}} \) as a function of \( R_0 \) and \( \sigma \) in Fig. 8.

Figure 8, combined with the instances of first fission from Figs. 4-7, place restrictions on where binary asteroid may be formed from YORP-induced break-up along the giant branch phases of stellar evolution. The times of first fission are independent of fragmentation prescription.

Strengthless rubble pile asteroids could form binary children for any parent radii where fission occurs: for example, for radii of several km at distances of a few au, 1 km at a couple tens of au, or 0.1 km at a couple hundreds of au. In contrast, the asteroids with the greatest internal strength, at \( \sigma = 10^3 \) Pa, are more restricted. For them, at a distance of a 5 au, there is only a narrow radii range of 1-5 km where binary formation is possible. At 30 au, the radii range is even narrower, between about 0.4-0.5 km. These results reinforce the notion that binary formation is more likely to occur at lower internal strengths. Nevertheless, if, like in the solar system, most asteroids in post-main-sequence planetary systems are strengthless rubble piles, then we might expect binary asteroid formation to be ubiquitous.

### 3 DISCUSSION

This large population of binary asteroids, however, may be short-lived. A bound binary asteroid created from YORP-induced fission will then be subject to the BYORP, or binary YORP, effect (Cuk & Burns 2005; Cuk 2007; Goldreich & Sari 2009; Walsh & Jacobson 2015). Unlike the YORP effect, the BYORP effect alters the binary orbit. Both the semimajor axis and eccentricity of the orbit vary secularly (McMahon & Scheeres 2010a) and their rates of change are linearly proportional to the stellar luminosity (McMahon & Scheeres 2010b).

In addition to BYORP, another driver of evolution which must be treated self-consistently is the mutual tidal interaction between the child asteroids. By assuming a constant Love number and constant stellar luminosity, Jacobson & Scheeres (2014) illustrated that when BYORP acts to shrink the semimajor axis and tides act to increase...
the semimajor axis, then the system could evolve towards an equilibrium state. Such a state provides a protection mechanism against destruction or escape, and hence allows the binary asteroid to be long-lived.

Determining whether equilibrium states could be maintained throughout and until the end of the giant branch phases of evolution would require detailed modelling. The stellar luminosity changes imply that the duration of an equilibrium state would be a function of when that state is achieved.

Perhaps the greater source of complication, however, is the effect of tides. The non-constancy of the Love number has important implications for tidal evolution (Efroimsky & Williams 2004; Efroimsky & Makarov 2013; Makarov & Efroimsky 2013; Correia et al. 2014; Boué et al. 2014). Even for a simple Maxwell rheology and when tides from one of the bodies can be neglected, the semimajor axis and eccentricity vary non-monotonically (Veras et al. 2019b). This behaviour would be complicated further by the addition of a force (such as BYORP) which couples to both the orbital and spin tidal equations of motion, as does, by analogy, the Lorenz force in other contexts (Veras & Wolszczan 2019).

Regardless of the lifetime of binary asteroid systems, the total number formed would be a strong function of the size of the monolithic constituents (such as boulders or grains) of the rubble pile asteroids. We can obtain some realistic number has important implications for tidal evolution. This investigation is only the second dedicated work after Veras et al. (2014c) (Paper I) to analyze aspects of the debris generated from giant branch YORP-based rotational fission, a process violent enough to pulverize entire Main Belt analogues in extrasolar systems.

Here we significantly expanded Paper I by considering multiple generations of fissions, incorporating internal strengths and demonstrating conditions for binary asteroid formation, all based on the analytical formalism of Scheeres (2018). Our key results are

(i) The final spin state is a weak function of stellar mass (Fig. 1).
(ii) Realistic nonzero internal strengths of rubble piles (up to 1 kPa) insufficiently protect asteroids against giant branch YORP-induced rotational fission (Fig. 2).
(iii) Successive fissions occur in progressively smaller time intervals as the star ascends the giant branches, despite the progressively faster failure spin rate (Fig. 3).
(iv) In most cases, there are either zero or more than ten fission events (or until the asteroid is broken down into its constituent boulders and grains); between one and ten fission events occur in only a narrow range of parameter space (Figs. 4-7).
(v) Binary asteroid formation from strengthless rubble piles is easy to generate and ubiquitous along the giant branch phases (Fig. 8), but the sustainability of that configuration until the white dwarf phase is in question (Section 3).

4 SUMMARY

Almost every known white dwarf planetary system features asteroidal debris, highlighting the critical need to understand how this debris is created during the giant branch phases of evolution. This investigation is only the second dedicated work after Veras et al. (2014c) (Paper I) to analyze aspects of the debris generated from giant branch YORP-based rotational fission, a process violent enough to pulverize entire Main Belt analogues in extrasolar systems.

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3 The total number of constituents is highly sensitive to $R_{\text{min}}$. If we neglect the $M_{\text{max}}$ terms in equation 16, then $N \propto R_{\text{min}}^{-3}$. 

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