NLO QCD corrections to pp → WW + jet + X

Stefan Dittmaier\textsuperscript{a}, Stefan Kallweit\textsuperscript{a} and Peter Uwer\textsuperscript{b} \textsuperscript{*}

\textsuperscript{a} Max-Planck-Institut für Physik (Werner-Heisenberg-Institut), D-80805 München, Germany
\textsuperscript{b} Institut für Theoretische Teilchenphysik, Universität Karlsruhe, D-76128 Karlsruhe, Germany

We report on a calculation of the next-to-leading order QCD corrections to the production of W-boson pairs in association with a hard jet at hadron colliders, which is an important source of background for Higgs and new-physics searches at the LHC. If a veto against the emission of a second hard jet is applied, the corrections stabilize the leading-order prediction for the cross section considerably.

1. Introduction

The search for new-physics particles—including the Standard Model Higgs boson—will be the primary task in high-energy physics after the start of the LHC that is planned for 2008. The extremely complicated hadron collider environment does not only require sufficiently precise predictions for new-physics signals, but also for many complicated background reactions that cannot entirely be measured from data. Among such background processes, several involve three, four, or even more particles in the final state, rendering the necessary next-to-leading-order (NLO) calculations in QCD very complicated. This problem led to the creation of an “experimenters’ wishlist for NLO calculations” \cite{1,2} that are still missing for successful LHC analyses. The process pp → W\textsuperscript{+}W\textsuperscript{−}+jet+X made it to the top of this list.

The process of WW+jet production is an important source for background to the production of a Higgs boson that subsequently decays into a W-boson pair, where additional jet activity might arise from the production or a hadronically decaying W boson \cite{3}. WW+jet production delivers also potential background to new-physics searches, such as supersymmetric particles, because of leptons and missing transverse momentum from the W decays. Besides the process is interesting in its own right, since W-pair production processes enable a direct precise analysis of the non-abelian gauge-boson self-interactions, and a large fraction of W pairs will show up with additional jet activity at the LHC. Last but not least WW+jet also delivers the real–virtual contributions to the next-to-next-to-leading-order (NNLO) calculation of W-pair production, for which further building blocks are presented in Ref. \cite{4}.

In these proceedings we briefly report on our recent calculation \cite{5} of NLO QCD corrections to WW+jet production at the Tevatron and the LHC, but here we discuss results for the LHC only. Parallel to our work, another NLO study \cite{6} of pp → W\textsuperscript{+}W\textsuperscript{−}+jet+X at the LHC appeared.

A tuned comparison of our results with results of Campbell et al. \cite{6} and Binoth et al. \cite{7} is in progress. Some details on the status of this comparison can be found in Ref. \cite{2}.

2. Details of the NLO calculation

At leading order (LO), hadronic WW+jet production receives contributions from the partonic processes qq → W\textsuperscript{+}W\textsuperscript{−}g, qg → W\textsuperscript{+}W\textsuperscript{−}q, and \bar{q}g → W\textsuperscript{+}W\textsuperscript{−}\bar{q}, where q stands for up- or down-type quarks. Note that the amplitudes for q =
u, d are not the same, even for vanishing light quark masses. All three channels are related by crossing symmetry. The LO diagrams for a specific partonic process are shown in Figure 1.

In order to prove the correctness of our results we have evaluated each ingredient twice using independent calculations based—as far as possible—on different methods, yielding results in mutual agreement.

2.1. Virtual corrections

The virtual corrections modify the partonic processes that are already present at LO. At NLO these corrections are induced by self-energy, vertex, box (4-point), and pentagon (5-point) corrections. For illustration the pentagon graphs, which are the most complicated diagrams, are shown in Figure 2 for a specific partonic channel. At one loop WW+jet production also serves as an off-shell continuation of the loop-induced process of Higgs+jet production with the Higgs boson decaying into a W-boson pair. In this subprocess the off-shell Higgs boson is coupled via a heavy-quark loop to two gluons.

Version 1 of the virtual corrections is essentially obtained as for the related processes of tH [8] and t̅t+jet [9] production. Feynman diagrams and amplitudes are generated with FeynArts 1.0 [10] and further processed with in-house Mathematica routines, which automatically create an output in Fortran. The IR (soft and collinear) singularities are treated in dimensional regularization and analytically separated from the finite remainder as described in Refs. [8,11]. The pentagon tensor integrals are directly reduced to box integrals following Ref. [12]. This method does not introduce inverse Gram determinants in this step, thereby avoiding numerical instabilities in regions where these determinants become small. Box and lower-point integrals are reduced à la Passarino–Veltman [13] to scalar integrals, which are either calculated analytically or using the results of Refs. [14]. Sufficient numerical stability is already achieved in this way, but further improvements with the methods of Ref. [15] are in progress.

Version 2 of the evaluation of loop diagrams starts with the generation of diagrams and amplitudes via FeynArts 3.2 [16], which is independent of version 1.0 [10]. The amplitudes are further manipulated with FormCalc 5.2 [17] and eventually automatically translated into Fortran code. The whole reduction of tensor to scalar integrals is done with the help of the LoopTools library [17], which also employs the method of Ref. [12] for the 5-point tensor integrals, Passarino–Veltman [13] reduction for the lower-point tensors, and the FF package [18] for the evaluation of regular scalar integrals. The dimensionally regularized soft or collinear singular 3- and 4-point integrals had to be added to this library. To this end, the explicit results of Ref. [11] for the vertex and of Ref. [19] for the box integrals (with appropriate analytical continuations) are taken.

2.2. Real corrections

The matrix elements for the real corrections are given by $0 \rightarrow W^+W^-q\bar{q}gg$ and
of the required colour and spin structures. The latter enter the evaluation of the dipoles in the Catani–Seymour subtraction method. The evaluation of the individual dipoles was performed using a C++ library developed during the calculation of the NLO corrections for $t\bar{t}$+jet \cite{29}. For the phase-space integration a simple mapping has been used where the phase space is generated from a sequential splitting.

### 3. Numerical results

We consistently use the CTEQ6 \cite{29} set of parton distribution functions (PDFs), i.e. we take CTEQ6L1 PDFs with a 1-loop running $\alpha_s$ in LO and CTEQ6M PDFs with a 2-loop running $\alpha_s$ in NLO. We do not include bottom quarks in the initial or final states, because the bottom PDF is suppressed w.r.t. to the others; outgoing $b\bar{b}$ pairs add little to the cross section\footnote{Sizeable contributions result from top-quark resonances in the subprocesses $pp \to W^+W^-q\bar{q}'q'$, which are usually treated as separate classes of processes.} and can be experimentally further excluded by anti-$b$-tagging. Quark mixing between the first two generations is introduced via a Cabibbo angle $\theta_C = 0.227$. In the strong coupling constant the number of active flavours is $N_F = 5$, and the respective QCD parameters are $\Lambda_5^{\text{LO}} = 165$ MeV and $\Lambda_5^{\text{MS}} = 226$ MeV. The top-quark loop in the gluon self-energy is subtracted at zero momentum. The running of $\alpha_s$ is, thus, generated solely by the contributions of the light quark and gluon loops. The top-quark mass is $m_t = 174.3$ GeV, the masses of all other quarks are neglected. The weak boson masses are $M_W = 80.425$ GeV, $M_Z = 91.1876$ GeV, and $M_H = 150$ GeV. The weak mixing angle is set to its on-shell value, i.e. fixed by $s^2_W = 1 - s^2_W = M_W^2/M_Z^2$, and the electromagnetic coupling constant $\alpha$ is derived from

\begin{table}[h]
\centering
\begin{tabular}{lccc}
process & $\sigma_{\text{LO}}$ [pb] & $\sigma_{\text{Sherpa}}$ [pb] & $\Delta\sigma$/stat. error \\
$pp \to WW + 1\text{jet} + X$ & 46.453(16) & 46.4399(94) & +0.70 \\
$pp \to WW + 2\text{jets} + X$ & 31.555(17) & 31.5747(63) & -1.08 \\
\end{tabular}
\caption{Comparison of LO cross sections with Sherpa (taken from Ref. \cite{27}).}
\end{table}
Fermi’s constant $G_\mu = 1.16637 \times 10^{-5}$ GeV$^{-2}$ according to $\alpha = \sqrt{2G_\mu M_W^2 s_w^2/\pi}$.

We apply the jet algorithm of Ref. [30] with $R = 1$ for the definition of the tagged hard jet and restrict the transverse momentum of the hardest jet by $p_{T,\text{jet}} > p_{T,\text{jet,cut}}$. In contrast to the real corrections the LO prediction and the virtual corrections are not influenced by the jet algorithm. In our default setup, a possible second hard jet (originating from the real corrections) does not affect the event selection, but alternatively we also consider mere WW+jet events with “no 2nd separable jet” where only the first hard jet is allowed to pass the $p_{T,\text{jet,cut}}$ but not the second.

Figure 3 shows the scale dependence of the integrated LO and NLO cross sections at the LHC for $p_{T,\text{jet,cut}} = 50$ GeV and 100 GeV. The renormalization and factorization scales are identified here ($\mu = \mu_{\text{ren}} = \mu_{\text{fact}}$), and the variation ranges from $\mu = M_W/10$ to $\mu = 10 M_W$. The dependence is rather large in LO, illustrating the well-known fact that the LO predictions can only provide a rough estimate. Varying the scales simultaneously by a factor of 4 (10) changes the LO cross section by about 35% (70%).

Only a modest reduction of the scale dependence to 25% (60%) is observed in the transition from LO to NLO if W pairs in association with two hard jets are taken into account. This large residual scale dependence in NLO, which is mainly due to qg-scattering channels, can be significantly suppressed upon applying the veto of having “no 2nd separable jet”. In this case the uncertainty is 10% (15%) if the scale is varied by a factor of 4 (10). The relevance of a jet veto in order to suppress the scale dependence at NLO was also realized [31] for genuine W-pair production at hadron colliders.

Further on, we show the integrated LO and NLO cross sections as functions of $p_{T,\text{jet,cut}}$ in Figure 4. The widths of the bands, which correspond to scale variations within $M_W/2 < \mu < 2 M_W$, reflect the behaviour discussed above for fixed value of $p_{T,\text{jet,cut}}$. For the LHC the reduction of the scale uncertainty is only mild unless WW+2jets events are vetoed.

Finally, Figure 5 shows the $p_{T,\text{jet}}$-distribution for the differential LO and NLO cross sections again both for $p_{T,\text{jet,cut}} = 50$ GeV and 100 GeV. Note that in the two plots the LO and the more inclusively defined NLO distributions are the same up to numerical fluctuations, whereas the more exclusive predictions differ in the two plots, since the veto applied on a second jet—which is not present for the two other curves—depends on the chosen value of $p_{T,\text{jet,cut}}$. For that reason com-
NLO QCD corrections to \( pp \to WW + jet + X \)

Figure 4. LO and NLO cross sections for WW+jet production at the LHC: dependence on \( p_{T,jet,cut} \) (taken from Ref. \[5\]).

\[
pp \to W^+W^- + jet + X \\
\sqrt{s} = 14 \text{ TeV} \\
0.5M_W < \mu < 2M_W
\]

\[
\sigma_{[pb]} \\
60 \quad 80 \quad 100 \quad 120 \quad 140 \quad 160 \quad 180 \quad 200
\]

\[ \text{LO (CTEQ6L1)} \]
\[ \text{NLO (CTEQ6M)} \]
\[ \text{NLO (CTEQ6M) no 2nd separable jet} \]

Figure 5. \( p_{T,jet} \)-distribution in LO and NLO for WW+jet production at the LHC: Here again we set renormalization and factorization scales equal to \( \mu = M_W \). The lower plot shows the \( K \)-factor for both definitions of the NLO observables. The curves for the LO and the more inclusive NLO cross section ("incl") agree in the \( p_{T,jet} \)-region covered by both plots, whereas the more exclusively defined NLO cross sections ("excl") differ due to the definition of the observable.
paring the $p_T, \text{jet}, \text{cut}$ plot of Figure 4 with a corresponding plot calculated by summing over the distributions of Figure 5 leads to agreement only in the observables with no veto on a second hard jet applied.

REFERENCES

1. C. Buttar et al., arXiv:hep-ph/0604120.
2. Z. Bern et al. [NLO Multileg Working Group], arXiv:0803.0494 [hep-ph].
3. B. Mellado, W. Quayle and S. L. Wu, Phys. Rev. D 76 (2007) 093007 [arXiv:0708.2507 [hep-ph]].
4. G. Chachamis, M. Czakon and D. Eiras, arXiv:0802.4028 [hep-ph] and arXiv:0806.3043 [hep-ph].
5. S. Dittmaier, S. Kallweit and P. Uwer, Phys. Rev. Lett. 100 (2008) 062003 [arXiv:0710.1577 [hep-ph]].
6. J. M. Campbell, R. K. Ellis and G. Zanderighi, arXiv:0710.1832 [hep-ph].
7. G. Sanguinetti and S. Karg, arXiv:0806.1394 [hep-ph]; T. Binoth, J.-P. Guillet, S. Karg, N. Kauer and G. Sanguinetti, in preparation.
8. W. Beenakker et al., Nucl. Phys. B 653 (2003) 151 [arXiv:hep-ph/0211352].
9. S. Dittmaier, P. Uwer and S. Weinzierl, Phys. Rev. Lett. 98 (2007) 262002 [arXiv:hep-ph/0703120].
10. J. Kühlbeck, M. Böhm and A. Denner, Comput. Phys. Commun. 60 (1990) 165; H. Eck and J. Kühlbeck, Guide to FeynArts 1.0, University of Würzburg, 1992.
11. S. Dittmaier, Nucl. Phys. B 675 (2003) 447 [arXiv:hep-ph/0308246].
12. A. Denner and S. Dittmaier, Nucl. Phys. B 658 (2003) 175 [hep-ph/0212259].
13. G. Passarino and M. Veltman, Nucl. Phys. B 160 (1979) 151.
14. G. ’t Hooft and M. Veltman, Nucl. Phys. B 153 (1979) 365; W. Beenakker and A. Denner, Nucl. Phys. B 338 (1990) 349; A. Denner, U. Nierste and R. Scharf, Nucl. Phys. B 367 (1991) 637.
15. A. Denner and S. Dittmaier, Nucl. Phys. B 734 (2006) 62 [arXiv:hep-ph/0509141].
16. T. Hahn, Comput. Phys. Commun. 140 (2001) 418 [hep-ph/0012260].
17. T. Hahn and M. Pérez-Victoria, Comput. Phys. Commun. 118 (1999) 153 [hep-ph/9807565]; T. Hahn, Nucl. Phys. Proc. Suppl. 89 (2000) 231 [hep-ph/0005029].
18. G. J. van Oldenborgh and J. A. M. Vermaseren, Z. Phys. C 46 (1990) 425; G. J. van Oldenborgh, Comput. Phys. Commun. 66 (1991) 1.
19. Z. Bern, L. J. Dixon and D. A. Kosower, Nucl. Phys. B 412 (1994) 751 [hep-ph/9306240].
20. S. Catani and M. H. Seymour, Nucl. Phys. B 485 (1997) 291 [Erratum-ibid. B 510 (1998) 503] [hep-ph/9605323].
21. S. Dittmaier, Phys. Rev. D 59 (1999) 016007 [arXiv:hep-ph/9805445].
22. F. A. Berends, R. Pittau and R. Kleiss, Nucl. Phys. B 424 (1994) 308 [hep-ph/9404313].
23. R. Kleiss and R. Pittau, Comput. Phys. Commun. 83 (1994) 141 [arXiv:hep-ph/9405257].
24. A. Denner et al., Nucl. Phys. B 560 (1999) 33 [arXiv:hep-ph/9904472].
25. W. Kilian, T. Ohl and J. Reuter, arXiv:0708.4233 [hep-ph].
26. T. Gleisberg et al., JHEP 0402 (2004) 056 [arXiv:hep-ph/03111263].
27. S. Kallweit, diploma thesis (in German), LMU Munich, 2006.
28. T. Stelzer and W. F. Long, Comput. Phys. Commun. 81 (1994) 357 [arXiv:hep-ph/9401258].
29. J. Pumplin et al., JHEP 0207 (2002) 012 [arXiv:hep-ph/0201195].
30. S. D. Ellis and D. E. Soper, Phys. Rev. D 48 (1993) 3160 [arXiv:hep-ph/9305266].
31. L. J. Dixon, Z. Kunszt and A. Signer, Phys. Rev. D 60 (1999) 114037 [arXiv:hep-ph/9907305].