A Thermodynamic Model for Water Activity and Redox Potential in Evolution and Development

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Abstract
Reactions involving water and oxygen are basic features of geological and biological processes. To understand how life interacts with its environment requires monitoring interactions with H₂O and O₂ not only at timescales relevant to organismal growth but also over billions of years of geobiological evolution. Chemical transformations intrinsic to evolution and development were characterized by analyzing data from recent phylostratigraphic and proteomic studies. This two-stage analysis involves obtaining chemical metrics (carbon oxidation state and stoichiometric hydration state) from the elemental compositions of proteins followed by modeling the relative stabilities of target proteins against a proteomic background to infer thermodynamic parameters [oxygen fugacity, water activity, and virtual redox potential (Eh)]. The main results of this study are a rise in carbon oxidation state of proteins spanning the time of the Great Oxidation Event, a rise in virtual redox potential that coincides with the likely emergence of aerobic metabolism, and a rise in carbon oxidation state of proteins inferred from the transcriptome in late stages of Bacillus subtilis biofilm growth. Furthermore, stoichiometric hydration state of expressed proteins decreases through stages of biofilm development, drops at the same time as a drop in organismal water content during fruit fly development, and is lower for proteins with more recent gene ages, all of which support the inference of higher hydration potentials at earlier time points. These results show how the evolutionary and developmental dynamics of major chemical variables can be deciphered through thermodynamic analysis of proteins as chemical entities.

Keywords Geochemical biology · Protein evolution · Biofilm development · Proteomics · Water activity · Oxidation state

Introduction
Many examples of dynamic hydration levels can be found in biology. Water content is one of the most basic biochemical quantities that changes during development (Church and Robertson 1966; Friis-Hansen 1983), and water is progressively lost from prenatal to adult forms in mammals (Logan and Himwich 1972; Calcagno et al. 1972; Friis-Hansen 1983). Conversely, relatively high water content has been recognized for over a century as a biochemical characteristic of cancer tissue (Cramer 1916; Downing et al. 1962; Saryan et al. 1974; Ross and Gordon 1982), and some authors have highlighted parallel trends of higher water content in both cancer and embryonic tissue (Winzler 1959; Olmstead 1966; McIntyre 2006). In origin-of-life research, geological environments with low water activity (a_H₂O) have been proposed to reduce or overcome the energetic barriers to polymerization of biomolecules in an aqueous environment (Pace 1991). This concept has received renewed attention recently for serpentinizing systems, which could provide not only oxidation-reduction (redox) disequilibria to drive the abiotic synthesis of various organic molecules but also pore spaces with reduced water activity (Lamadrid et al. 2017).

The importance of both redox conditions and water activity for life’s origin in geological environments (do Nascimento Vieira et al. 2020), not to mention the fact that water is involved in far more biochemical reactions than any other metabolite (Frenkel-Pinter et al. 2021), raises the question of whether biological processes in general are also shaped by these chemical parameters. With the growing availability of evolutionary gene-age
estimates and measurements of protein abundance during organismal development, it is now possible to construct thermodynamic models for chemical transformations of the most abundant type of biomacromolecule—that is, proteins—that occur at timescales longer than cellular lifetimes.

Thermodynamic principles predict the most stable chemical species, but do not say how the reactions that lead to them take place (Bard 1986). Relative stability diagrams for minerals, also known as chemical activity or predominance diagrams, are immensely useful for interpreting geological phenomena, yet are agnostic about nucleation effects or whether the minerals grow through precipitation from solution or solid-state diffusion and replacement. This is because it is only the Gibbs energy of the system, and not any particular reaction mechanism, that determines the relative stabilities of chemical species.

In the same way that stability diagrams for mineral phases neither inform nor conflict with mechanistic models of nucleation or precipitation and replacement reactions, an analogous thermodynamic depiction of protein sequences does not conflict with elementary biochemical models of ATP conjugation and amino acid synthesis and polymerization. Such a model is likewise ambivalent about biological mechanisms at all levels from DNA replication and mutation to protein function, survival, and natural selection. By saying nothing about these mechanisms, the model independently predicts which proteins are more stable in a multidimensional space defined by temperature, pressure, and chemical potentials—the fundamental variables in thermodynamics.

The consideration of both water activity and oxygen fugacity ($f_{O_2}$)—a thermodynamic indicator of oxidation potential—is essential for thermodynamic models of melting and magmatic processes (Foley 2011) as well as low-temperature metasomatic processes including serpentinization (Evans et al. 2013). Although $f_{O_2}$ may have no physical meaning as an indicator of partial pressure, it has a thermodynamic definition that makes it a useful indicator of the internal oxidation potential of systems without an actual gas phase (Frost 1991). For instance, an oxygen fugacity given by $\log f_{O_2} = -65$ (where log denotes the common logarithm) is many orders of magnitude lower than an estimated upper bound of partial pressure of $O_2$ in the prebiotic Archean near-surface atmosphere ($< 10^{-13}$ bar; Kasting 1993; Catling and Claire 2005), and would correspond to one molecule of $O_2$ in a volume approximately equal to that of the solar system (Anderson 2005, p. 365). Despite its unphysical interpretation as a scale of partial pressure, $f_{O_2}$ can be converted to meaningful values of redox potential in the $Eh$ scale. By way of example, for unit activity of water (that is, $\log a_{H_2O} = 0$), values of $\log f_{O_2}$ between $-60$ and $-83.1$ correspond to $Eh$ values between approximately $-72$ and $-414$ mV at pH 7 and 25 °C (Garrels and Christ 1965, p. 176).

Inorganic geochemistry is primarily concerned with reactions among minerals and dissolved aqueous species; geochemical biology, as envisioned in this study, applies the same concepts to groups of proteins that constitute an evolutionary or developmental series. The thermodynamic model here is parameterized in terms of water activity and oxygen fugacity, which are then converted to the $Eh$ scale of redox potential that is more common in biology. This method offers a path toward quantitative thermodynamic retrodiction of past redox conditions by comparing groups of proteins classified by the evolutionary ages of genes (phylotastra). Similarly, a chemical representation of developmental patterns of protein expression provides novel insight into the role of water at the nexus between protein expression and cell physiology.

**Materials and Methods**

**Chemical Metrics**

Two chemical metrics derived from the elemental compositions of proteins are used in this study. This chemical representation is the precursor to a thermodynamic analysis that provides a theoretical assessment of redox potential and water activity.

Carbon oxidation state ($Z_C$) represents the average charge on carbon atoms in a molecule, given nominal charges of the other atoms ($H^{+1}, N^{-3}, O^{-2}, S^{-2}$). The carbon oxidation state can be computed directly from the elemental abundances of molecules in which the heteroatoms (N, O, S) are bonded only to H and/or C but not to each other (Dick 2014; Dick et al. 2020). This condition holds for the 20 standard amino acids and for primary sequences of proteins but not for disulfide bonds and some types of post-translational modifications, none of which are considered here.

Stoichiometric hydration state ($n_{H_2O}$) is the coefficient on $H_2O$ in the mass-balanced reaction representing the theoretical formation of a protein from a set of thermodynamic components, also known as basis species. Any set of components that represents the compositional variability of a system using the minimum number of components is acceptable, and the choice of a particular set is determined only by convenience (Gibbs 1876, p. 117). Thus, components may be chosen that aid the visualization of compositional differences on two-dimensional diagrams, which have a precise geometric relation to field boundaries on chemical potential diagrams (Helgeson 1968). The basis species glutamine, glutamic acid, cysteine, $H_2O$, and $O_2$ (denoted “QEC”) were used in this and other recent studies (Dick et al. 2020; Dick 2021). This particular choice of basis species was made to (1) strengthen the covariation between two measures of oxidation state: $Z_C$ (which does not depend on the choice
of basis species) and the number of $O_2$ in the theoretical formation reactions of proteins from basis species, and (2) reduce the covariation between $Z_C$ and $n_{H_2O}$. By contrast, when used as basis species for protein formation reactions, a selection of inorganic species that are commonly used to balance overall metabolic reactions ($CO_2$, $NH_3$, $H_2S$, $H_2O$, $O_2$) displays a negative correlation between $n_{H_2O}$ and $Z_C$ that is stronger than the positive correlation found between $n_{O_2}$ and $Z_C$ (Fig. 1). The large negative slope dominates the differences between proteins, making it very difficult to disentangle distinct trends in oxidation and hydration state.

Because a projection onto two variables is determined by the chemical formulas of all of the basis species, some basis sets strongly couple the $O_2$ and $H_2O$ components while others do not. In a previous study, the QEC basis species were selected by computing $n_{H_2O}$ and $n_{O_2}$ from the overall formation reactions of the 20 protein-forming amino acids from all possible sets of three amino acids together with $H_2O$ and $O_2$ and analyzing their correlations with $Z_C$. Several candidate

![Fig. 1 Comparison of two possible sets of basis species for the theoretical formation reactions of proteins. Amino acid compositions of proteins were obtained from the Homo sapiens (Hsa) UniProt reference proteome (The UniProt Consortium 2019) downloaded on 2016-04-03 (UP000005640) and from the Drosophila melanogaster (Dme) and Bacillus subtilis (BsU) reference proteomes downloaded on 2021-07-12 (UP00000803 and UP000001570). Chemical metrics were normalized by number of carbon atoms ($Z_C$) or by number of amino acid residues ($n_{O_2}$ and $n_{H_2O}$) and values were plotted using the smoothScatter() function in R (R Core Team 2021) to generate a smoothed kernel density estimate of the data represented by color intensity. Small black symbols indicate the first 100 points in the low-density areas. Glutamine, glutamic acid, cysteine, $H_2O$, and $O_2$ are referred to in the text as the QEC basis species. A second set of basis species, $CO_2$, $NH_3$, $H_2S$, $H_2O$, and $O_2$, includes major inorganic reactants in autotrophic metabolism (Wimmer et al. 2021), except that $O_2$ was swapped for $H_2$. Of the two sets of basis species, QEC exhibits a stronger positive correlation between $n_{O_2}$ (a metric of oxidation state derived from formation reactions) and $Z_C$ (a metric of oxidation state derived from chemical formulas that is independent of the choice of basis species) and at the same time greatly reduces the correlation of $n_{H_2O}$ (a metric of hydration state) with $Z_C$. Linear fits are indicated by dashed gray lines and $R^2$ values. The plots for human proteins without the linear fits were previously published in the Supplemental Information of Dick (2017) (license: CC-BY 4.0)
sets of basis species have similarly strong $n_{O_2}$–$Z_C$ and weak $n_{H_2O}$–$Z_C$ correlations; from these, QEC was selected because these amino acids are relatively biologically abundant and are highly connected in metabolic networks (see Dick et al. 2020 for details). By projecting elemental formulas of proteins using the QEC basis species, $Z_C$ and $n_{H_2O}$ can be regarded as largely uncoupled variables that enable changes of oxidation and hydration state to be identified as nearly perpendicular trends on $n_{H_2O}$–$Z_C$ scatterplots.

In order to represent chemical differences associated with amino acid composition, values of $n_{H_2O}$ for individual proteins were normalized by protein length. To illustrate the necessity for normalization, a 200-aa protein has more O and H atoms than a 100-aa protein, so the number of $H_2O$ molecules in the theoretical formation reaction is greater for the larger protein. With normalization, differences of $n_{H_2O}$ between proteins are not dominated by protein length, but instead represent differences in amino acid composition. In contrast, because $Z_C$ is defined as a per-carbon quantity, it does not scale with protein length, and normalizing it by protein length would be inappropriate.

Chemical metrics ($Z_C$ and $n_{H_2O}$) for individual proteins were used to calculate mean values and bootstrap confidence intervals for groups of proteins. The calculations were performed either without weighting (for phylolstratigraphic datasets or proteomic datasets that list up-and-down-regulated proteins) or with weighting by abundance (for proteomic or transcriptomic datasets that give expression levels). Means of chemical metrics were not weighted by protein length, so large and small proteins contribute equally to the mean value. To calculate thermodynamic parameters ($\log f_{O_2}$ and $\log a_{H_2O}$), each group of proteins was modeled by a single target protein having the mean amino acid composition of the group. In contrast to the mean values for chemical metrics, the mean amino acid compositions for target proteins include weighting by both abundance (if available) and implicitly by protein length, as longer proteins have more amino acid residues.

### Data Sources

Phylostraata were obtained from the supporting information of Trigos et al. (2017) and the “main_HUMAN.csv” file of Liebeskind et al. (2016a, 2016b). The Ensembl gene identifiers in the Trigos et al. dataset were converted to UniProt accession numbers (The UniProt Consortium 2019) using the UniProt mapping tool (Huang et al. 2011); 169 of 17,318 genes could not be mapped to UniProt and were removed from the subsequent analysis.

Transcriptomic and proteomic data for growing *Bacillus subtilis* biofilms were taken from Supplementary file S10 of Futo et al. (2021), specifically the tables named “Input values for calculating TAI” and “Input values for calculating PAI.” The phylostraata given by Futo et al. (2021) were not included in this analysis. Data for the developmental proteome of *Drosophila melanogaster* were extracted from Supplemental Table S1 of Casas-Vila et al. (2017). The values in the columns for imputed log$_2$ LFQ intensity were exponentiated, then mean values were computed for each time point (4 replicates). For both the *B. subtilis* and *Drosophila* datasets, protein IDs were mapped using the UniProt mapping tool (Huang et al. 2011). The canonical protein sequences were downloaded from UniProt, and the read.fasta() function in the CHNOSZ package (Dick 2019) was used to compute the amino acid compositions of the proteins.

Differentially expressed proteins between embryos and adult flies were obtained from Supplementary Table S2 of Fabre et al. (2019). After rounding the values in the “Log2 ratio Adult/Embryo” column to 2 decimal places and those in the “$-\log 10$ BH corrected $p$ value Adult vs Embryo” column to whole numbers, the table was filtered to include proteins with log$_2$ expression change $\geq 1$ or $\leq -1$ and log$_{10}$ $p$ value $\leq 2$. This yielded 407 and 369 proteins with higher expression in adults and embryos, respectively; these are very close to the numbers given by Fabre et al. (2019) (407 and 371 proteins enriched in adults and embryos).

### Computer Code

All figures were created in R version 4.1.2 (R Core Team 2021). The R package CHNOSZ version 1.4.2 (Dick 2019) was used for thermodynamic calculations, and canprot version 1.1.2 (Dick 2021) was used for calculating chemical metrics from amino acid compositions of proteins. The R package boot version 1.3–28 (Canty and Ripley 2021; Davison and Hinkley 1997) was used for calculating bootstrap confidence intervals (95% confidence levels of the percentile type for 999 bootstrap replicates).

### Results

#### Scope and Limitations of Phylostratigraphic Datasets

Phylostraata represent conservation levels of orthologous genes in a phylogenetic tree (Domazet-Lošo et al. 2017; Van Oss and Carvunis 2019). Although the complex sequence of evolutionary events for any gene precludes a single, well-defined age, an operational definition used in phylostratigraphy considers the presence or absence of a gene family in different species (i.e., Dollo parsimony), leading to the inference that the gene family originated in the most recent common ancestor of all species that have that gene family (Capra et al. 2013). Accordingly, applications of phylostratigraphic analysis often refer to the evolutionary
age of particular genes (Trigos et al. 2017; Zhou et al. 2018; Futo et al. 2021). However, true orthologs that cannot be detected (false negatives) become more common with greater evolutionary divergence (Natsidis et al. 2021), which adds to the uncertainty of phylostratigraphic age estimates.

Homology detection based on protein domains can reduce false negatives compared to that based on full gene sequences. Sensitivity can also be increased by using hidden Markov models for multiple sequences (instead of pairwise sequence alignment), and statistical power is enhanced by analyzing the full genomes of hundreds of species rather than particular focal species. By using these techniques, James et al. (2021) found that the support for phylostratigraphic trends in protein hydrophobicity and intrinsic structural disorder was strengthened compared to previous studies. Accordingly, although false negatives may have been more prevalent in earlier phylostratigraphic studies, they are probably random errors that do not create spurious trends, but simply reduce the power to detect trends. It was also noted that ancient domains are strongly influenced by the amino acid availability at the time of de novo gene birth, even after billions of years of evolution (James et al. 2021). The preservation of ancient patterns of amino acid composition in contemporary sequences supports the approach used in the present study of comparing the chemical metrics for proteins in different age groups to geological events.

A further limitation is that phylostratigraphy represents ages of genes in a particular species (Natsidis et al. 2021). Therefore, phylostra with age into species and do not yield complete ancestral proteomes. For human genes, the number of genes assigned to particular phylostrata varies widely (Fig. 2); in the dataset of Trigos et al. (2017) there are as many as 4665 for PS 2 (Eukaryota) and as few as 25 for PS 16 (Homo sapiens) (these counts exclude 10 genes in each of those phylostrata that could not be mapped to UniProt IDs). Therefore, the chemical analysis performed here only characterizes subsets of proteins associated with particular phylogenetic branches, and not entire proteomes.

Another limitation of this analysis is that actual expression levels vary dramatically for different proteins, but phylostratigraphic datasets do not provide any abundance information. In the second part of this study, protein expression levels are used to construct abundance-weighted means of chemical metrics and amino acid composition for developmental proteomes. Such an abundance-weighted mean is not possible for the chemical and thermodynamic analysis of phylostratigraphic data.
Chemical Analysis of Proteins in Phylostratigraphic Age Groups

The mean lengths of proteins coded by genes in each of 16 phylostrata (PS) for human protein-coding genes given by Trigos et al. (2017) are plotted in Fig. 2a. There is an initial rise in protein length leading up to Eukaryota, which is consistent with the previously reported greater median protein length in eukaryotes than prokaryotes (Brocchieri and Karlin 2005). Although it is debated whether the large decline of protein length for younger genes (i.e., those with lower conservation levels) is real (Lipman et al. 2002; Domazet-Lošo et al. 2017) or to some extent an artifact of BLAST-based homology detection (Moyers and Zhang 2017; Van Oss and Carvunis 2019), controlling for length either strengthens or has no effect on inferred trends of intrinsic structural disorder (ISD) (Wilson et al. 2017; Heames et al. 2020). ISD predicted from amino acid sequences of proteins is strongly associated with hydrophobicity (James et al. 2021); similarly, the chemical metrics used here are derived from the amino acid compositions of proteins, and Z_C exhibits a negative correlation with amino acid hydrophobicity (Dick 2014), so trends in these metrics are likely to be robust against length-dependent artifacts.

Figure 2a reveals distinct evolutionary patterns of oxidation state and hydration state of proteins. Z_C forms a strikingly smooth hump between PS 1 and 11 then increases rapidly to the maximum at PS 14, followed by a smaller decline to PS 16, which corresponds to Homo sapiens. In contrast, n_H2O shows an overall decreasing trend toward younger phylostrata, although there are positive jumps between PS 3 and 4 and PS 7 and 8.

Figure 2b shows the same analysis applied to proteins grouped into eight gene ages (GA) reported by Liebeskind et al. (2016b) based on consensus tables of gene-age estimates from different orthology inference algorithms. The gene ages of Liebeskind et al. have three steps between cellular organisms and Eukaryota, providing a greater resolution in earlier evolution compared to the phylostrata of Trigos et al., and stop at Mammalia, which corresponds to PS 10 of Trigos et al. Keeping in mind the different resolutions and scales of the Trigos et al. phylostrata and Liebeskind et al. gene ages, the two datasets show similar maxima for Z_C and protein length between the origins of Opisthokonta and Eumetazoa, and an overall decrease of n_H2O in younger age groups (Fig. 2b).

The Great Oxidation Event refers to the rise of atmospheric oxygen, originally thought of as a single-step increase between 2.45 and 2.32 billion years ago to 1–40% of present levels (Kump 2008), but now recognized as an approach to near-modern levels followed by a plunge (Lyons et al. 2014). Therefore, the organic processes required for the origin of cellular organisms at ca. 4.290 Mya and for the emergence of eukaryotes at 2101 Mya (divergence times from Kumar et al. 2017) must have taken place under vastly different oxygen regimes.

If Earth’s oxygenation is thermodynamically linked to the oxidation state of proteins, then a rise in Z_C should be apparent for multiple lineages, not only the human one represented in Fig. 2. To investigate the Z_C trends in other eukaryotic lineages, additional phylostratigraphic data were analyzed for 31 model organisms representing opisthokonts (fungi, animals, and some protists) studied by Liebeskind et al. (2016b) and for homology groups from 435 fully sequenced animal, plant, and fungal species reported by James et al. (2021). For every opisthokont, mean Z_C of proteins in phylostratigraphic age groups shows an overall increase between cellular organisms (GA 1) and Eukaryota (GA 4) and continues to increase to Opisthokonta (GA 5). For later age groups, the lineages of the included organisms diverge, as do their Z_C trends (Fig. 3a). For homology groups in 435 species, Z_C of non-transmembrane protein domains increases with a fitted slope of 0.015 to 0.018 Gya⁻¹ in plants and animals (Fig. 3b). This is comparable to a rise of ca. 0.019 Z_C/Gya in the human lineage leading up to the emergence of opisthokonts at 1105 Mya (Fig. 3a). Therefore, the carbon oxidation state of new proteins in multiple eukaryotic lineages likely increased over an interval spanning the Great Oxidation Event.

Thermodynamic Model for Maximum Activities of Proteins

To take the step from chemical composition to chemical potential, a thermodynamic model is described here for predicting the oxidation and hydration potentials that stabilize particular proteins compared to others. This analysis of relative stability does not refer to the forces that determine protein conformations (i.e., 3-dimensional structures), but to the Gibbs energies of the theoretical formation reactions of proteins from basis species. It follows that the relative stabilities of proteins are influenced by the chemical activities of basis species whose stoichiometric coefficients depend on the elemental abundances and therefore amino acid sequences of different proteins.

To give a worked-out example, the balanced formation reaction of a well-known protein, chicken egg-white lysozyme (UniProt: P00698, LYSC_CHICK), can be written as

\[
0.5144\text{Gln} + 0.3892\text{Glu} + 0.0780\text{Cys} = C_{4.752}H_{7.434}N_{1.496}O_{4.134}S_{0.078} + 0.8794\text{H}_2\text{O} + 0.4713\text{O}_2 \tag{R1}
\]

Here, the chemical formula of the whole protein (C_{613}H_{959}N_{193}O_{185}S_{10}) is divided by the protein length (129) to give the per-residue formula that is a product of the reaction. The only other species in the reaction are the basis...
Carbon oxidation state of proteins is higher for younger proteins in eukaryotic lineages. A Mean protein $Z_c$ was computed for consensus gene ages of the 31 model organisms in Table 1 of Liebeskind et al. (2016b). All these organisms are opisthokonts (commonly characterized by flagellate cells and formerly known as the Fungi/Metazoa group), so they have a common ancestry up to GA 5, but their lineages diverge for later gene ages. Names of age categories and number of organisms are shown below the plot; the upper labels give the divergence times for the human lineage (Kumar et al. 2017), which is highlighted in red in the plot. B $Z_c$ calculated for amino acid compositions of protein homology groups generated by James et al. (2021). In that study, protein sequences were obtained from 435 genomes, protein domains were annotated using the Pfam database (El-Gebali et al. 2019) and were used to construct homology groups representing the average for each Pfam, and age assignments of Pfam domains were made using TimeTree (Hedges et al. 2006) with exceptions for LUCA and domains that emerged after LUCA but before eukaryotes. Numbers of homology groups are given in the plot titles, and box widths are proportional to the square root of number of groups for each age. Horizontal dashed gray lines indicate the median value for LUCA in each plot. Data were obtained from the AAcomp_pfam_*.csv files for untransformed amino acid proportions in HomologyDictionaryFiles.zip downloaded from Figshare (James et al. 2020).

![Divergence times for human lineage (Mya)](image)

$1$ Cellular organisms (31)
$2$ Euk_Archaeba (31)
$3$ Euk+Bac (31)
$4$ Eukaryota (31)
$5$ Opisthokonta (31)
$6$ Bikarya (9), Eumetazoa (21)
$7$ Ascomycota (7), Basidiomycota (2), Protostomia (5), Vertebrata (13)
$8$ Ecdysozoa (4), Mammalia (9), Saccharomycota (6), Teleostei (2)
$9$ Arthropoda (3)

Species glutamine ($\text{C}_5\text{H}_1\text{N}_2\text{O}_3$), glutamic acid ($\text{C}_5\text{H}_9\text{NO}_4$), cysteine ($\text{C}_3\text{H}_7\text{NO}_3\text{S}$), $\text{H}_2\text{O}$, and $\text{O}_2$. The coefficient on $\text{H}_2\text{O}$ in this reaction is the opposite of the stoichiometric hydration state; that is, $n_{\text{H}_2\text{O}} = -0.879$. The carbon oxidation state of the protein, $Z_C = 0.016$, can be computed from either its chemical formula or amino acid composition (see Dick et al. 2020).

The central thermodynamic quantity in this model is chemical affinity ($\Delta H$), which is the opposite of the non-standard Gibbs energy change of the reaction (Denbigh 1981, p. 143) and can be computed from (e.g., Solel et al. 2019)

$$\Delta H = -\Delta G = 2.303RT \log(K/Q),$$  

(1)

where $K$ is the equilibrium constant and $Q$ is the activity product for the formation reaction for a particular protein. Factorization using the natural logarithm of 10 ($\approx 2.303$) means that common logarithms of variables are used throughout. Because it includes the chemical activities of all the species in the reaction, $Q$ is affected by both $f_\text{O}_2$ and $\rho_{\text{H}_2\text{O}}$, which represent oxidation and hydration potential, while $K$ is a function of the standard Gibbs energy of the reaction and therefore of temperature and pressure.

The standard Gibbs energies ($\Delta G^\circ$) of proteins were calculated using amino acid group additivity as described by Dick et al. (2006) together with later updates for methionine and glycine groups and the protein backbone (LaRowe and Dick 2012; Kitadai 2014). For the purpose of quantifying the relative stabilities of proteins in terms of hydration and oxidation potential, the calculations were limited to proteins treated as neutral species using values of $\Delta G^\circ_f$ calculated for $25^\circ\text{C}$ and 1 bar. For each protein, $\Delta G^\circ_f$ was also divided by the protein length to obtain the per-residue value, which was combined with the standard Gibbs energies of the other
species in the reaction to calculate the standard Gibbs energy of reaction \(\Delta G^\circ\), and from that, \(\log K\). The standard Gibbs energies for \(H_2O\), \(O_2\), and amino acids were taken from Haar et al. (1984), Wagman et al. (1982), and Dick et al. (2006). By using the subcrt() function in the CHNOSZ package (Dick 2019), \(\log K\) for Reaction (R1) at 25°C and 1 bar can be computed to be \(-39.84\).

Calculation of the activity product \(Q\) requires values for activities of all the species in the reaction; because oxygen is a gas, the fugacity of \(O_2\) is used instead of activity. \(\log a_{H_2O}\) and \(\log f_{O_2}\) were chosen as the descriptive variables, so their values correspond to the axes of a 2-dimensional grid (256 × 256 resolution) used to plot the relative stabilities of the proteins. Although the chemical activities of all the basis species could be varied in the thermodynamic model, it is not feasible to produce a 5-dimensional visualization of the system. Therefore, the activities of the other basis species were set to constants that correspond to biochemically reasonable concentrations. Specifically, mean concentrations of amino acids in human plasma (Tcherkas and Denisenko 2001) were used; expressed as logarithms of concentrations in mol/L, these are \(-3.2\) for glutamine, \(-4.5\) for glutamic acid, and \(-3.6\) for cysteine. Finally, the activity of the per-residue formula for each protein was set to unity. The activities were combined to give values of \(Q\) that were then used to calculate chemical affinity from Eq. (1). Continuing the example for LYSC_CHICK, \(\log Q\) for Reaction (R1) at nominal values of \(\log f_{O_2}\) (−70) and \(\log a_{H_2O}\) (0) is \(-29.33\), which yields \(\log(K/Q) = -10.52\).

The relative stabilities of proteins represented by their per-residue formulas were computed by using the Boltzmann distribution written as

\[
\frac{a_i}{\sum a_i} = \frac{e^{\lambda_i/RT}}{\sum e^{\lambda_i/RT}},
\]

where \(a\) is activity, \(A\) is affinity calculated given unit activity of the per-residue formula for each protein, and \(i\) designates a single protein in a system of any number of proteins. Activity coefficients were taken to be unity, and the total activity \(\sum a_i\) was also fixed at unity. Consequently, \(a_i\) for each protein represents its fractional abundance at equilibrium with all other proteins in the system. This metastable equilibrium model for the relative abundances of proteins does not inform about the total equilibrium state of the system.

According to the equilibrium model, each protein in a system of candidate proteins has a finite value of activity that depends on \(\log a_{H_2O}\) and \(\log f_{O_2}\), which are the only free variables. The predominant protein for any combination of these variables (“condition”) is the one with the highest predicted activity. In thermodynamic models for inorganic systems, analogous calculations are used to make predominance diagrams for aqueous species (e.g., Kinniburgh and Cooper 2004), but for the analysis of biological data it is more informative to find the sets of conditions that, respectively, maximize the activity of each of the proteins in a system and not only the predominant one. This model, which is referred to as “MaximAct” in the present study, is described next.

Maximizing Stabilities of Target Proteins on a Proteomic Background

In order to thermodynamically characterize the differences in protein composition between phylostrata, model proteins for each phylostratum (referred to here as target proteins) were generated by computing the mean amino acid composition of all proteins in each phylostratum. Equilibrium calculations for the 16 target proteins for the Trigos et al. phylostrata are displayed on the \(\log a_{H_2O} - \log f_{O_2}\) diagram in Fig. 4a. Predominance fields for just a few proteins are visible on the diagram. These fields represent the proteins that have the highest activities; those with lower activity do not predominate, but they still have calculable values of chemical activity. The conditions for maximum activity for each of the 16 target proteins (indicated by the points) are found at extreme values of \(\log a_{H_2O}\) and \(\log f_{O_2}\). Finite conditions for maximum activity of some of the proteins could be found by extending the range of the diagram, but the activities of the predominant proteins maximize at infinite values of \(\log a_{H_2O}\) and/or \(\log f_{O_2}\). Therefore, it is not possible to use this simple model to find particular values of water activity and oxygen fugacity that characterize each phylostratum.

A key innovation in this study is the addition of more proteins to the thermodynamic system to represent a background population, or biological context, that allows the transformations between target proteins to be resolved in finer detail. An appropriate set of background proteins would have a wider compositional range than the mean amino acid compositions used to make the target proteins. Because the background proteins are now competing for formation with the target proteins, the conditions for maximum activity of the latter will be constrained to smaller and more meaningful ranges of \(\log a_{H_2O}\) and \(\log f_{O_2}\). The background proteins should also represent the actual biological range of amino acid composition, so a plausible choice is to use all the proteins coded by the human genome. To reduce model bias that could be caused by the inclusion of background proteins with unusual amino acid compositions, a representative human proteome background was constructed by taking the intersection of UniProt IDs for proteins coded by genes in the Trigos et al. and Liebeskind et al. datasets, yielding 16,723 unique sequences.

The calculated predominance diagram for a system of 16 target proteins together with 200 randomly sampled background proteins reveals that a relatively small number of background proteins predominate at equilibrium (Fig. 4b).
None of the 16 target proteins predominates, but instead their activities are maximized at particular values of $\log a_{\text{H}_2\text{O}}$ and $\log f_{\text{O}_2}$. Figure 4b is a result that corresponds to only one random subsample of the background human proteome. There are many possible versions of Fig. 4b, which are not shown here. Instead, the $\log a_{\text{H}_2\text{O}}$ and $\log f_{\text{O}_2}$ values obtained by using many random subsamples of the human proteome with a larger number of sampled proteins (2000) are shown in Fig. 5a and b. This number was chosen to be able to run the calculation within computer memory limits, and the random subsampling was repeated 100 times to obtain mean values for $\log a_{\text{H}_2\text{O}}$ and $\log f_{\text{O}_2}$, which approximate the values that would be obtained if a single calculation could be performed with all 16,723 proteins in the background proteome.

The variability among calculations displayed in Fig. 5a and b is due to the limited subsample size of background proteins, not to intrinsic biological variability. The use of a single mean amino acid composition for each target protein precludes the calculation of confidence intervals for thermodynamic parameters ($\log a_{\text{H}_2\text{O}}$ and $\log f_{\text{O}_2}$), but relative uncertainties within datasets may be assessed by comparison with the confidence intervals for the corresponding chemical metrics.

It is not surprising to find that the trends of $\log a_{\text{H}_2\text{O}}$ and $\log f_{\text{O}_2}$ depicted in Fig. 5a and b are similar to those of the corresponding chemical metrics, $n_{\text{H}_2\text{O}}$ and $Z_C$, in Fig. 2a. For instance, PS 1 (cellular organisms) has both the highest $n_{\text{H}_2\text{O}}$ and $\log a_{\text{H}_2\text{O}}$. It is noteworthy that the water activity for PS 2–10 predicted by the MaximAct model fluctuates around unity, which is indicated by the horizontal dot-dashed line at $\log a_{\text{H}_2\text{O}} = 0$ in Fig. 5c. Between PS 10 (Mammalia) and PS 15 (Homininae), both $n_{\text{H}_2\text{O}}$ and $\log a_{\text{H}_2\text{O}}$ decrease considerably. However, although PS 16 (Homo sapiens) has the lowest $n_{\text{H}_2\text{O}}$ of any phylostratum (Fig. 2a), the thermodynamic model predicts a higher $\log a_{\text{H}_2\text{O}}$—closer to 0—for PS 16 compared to PS 15. Looking at the oxidation trends, the broad hump in $Z_C$ between PS 1 and 11 is reflected in $\log f_{\text{O}_2}$ values but with a more rugged profile, and PS 11 (Theria) has both the lowest $Z_C$ and lowest $\log f_{\text{O}_2}$ (Fig. 5b).

**Virtual Redox Potential**

Oxygen fugacity is a thermodynamic quantity that implies nothing about the actual mechanism of oxidation or reduction (Anderson and Crerar 1993) and in practice is used to calculate other parameters that are easier to measure (Anderson 2005, p. 245). In this study, the theoretical values of not only $\log f_{\text{O}_2}$ but also $\log a_{\text{H}_2\text{O}}$ are used to calculate virtual redox potential ($E_h$) for comparison with experimental measurements of $E_h$. The qualifier “virtual” signifies that the calculated values of $E_h$ are not obtained from standard laboratory techniques, but rather from an independent
Fig. 5 Analysis of optimal water activity and oxygen fugacity for phylostrata and calculation of virtual redox potential (Eh). a and b Values of log$a_{H_2O}$ and log$f_{O_2}$ that maximize the activity of target proteins for the Trigos et al. phylostrata in metastable equilibrium with each other and 2000 randomly sampled background proteins. Each thin gray line represents a calculation for one random sample, and thick red lines show the means for 100 calculations. c Comparison of mean values of log$a_{H_2O}$ with pure water (horizontal dot-dashed line at log$a_{H_2O} = 0$). Vertical lines at cellular organisms, Eukaryota, Eumetazoa, and Mammalia indicate coinciding gene ages in the Liebeskind et al. dataset. The shaded gray area represents phylostrata that postdate the emergence of Mammalia, which are not available in the Liebeskind et al. dataset. d Virtual Eh calculated from the mean values of log$a_{H_2O}$ and log$f_{O_2}$ using Eqs. (3–4) (thick red line) and from the same values of log$f_{O_2}$ with log$a_{H_2O} = 0$ (dashed red line). Horizontal dotted lines represent redox potentials for the glutathione redox couple (GSSG/GSH) measured in human blood plasma (Jones and Sies 2015) and in whole cell lysates or monitored with fluorescent protein sensors in the cytosol and endoplasmic reticulum (ER) of multiple cell lines (Schwarzländer et al. 2016). e and f Analogous calculations of log$a_{H_2O}$ and Eh using the Liebeskind et al. gene ages; vertical lines represent cellular organisms, Eukaryota, Eumetazoa, and Mammalia.

thermodynamic model for the chemical differences of proteins over evolutionary and developmental time scales.

Virtual redox potential was calculated by considering the half-cell reaction for H$_2$O:

$$H_2O = 0.5O_2 + 2H^+ + 2e^-.$$  \hspace{1cm} (R2)

For equilibrium of Reaction (R2), we can write

$$\log K = 0.5 \log f_{O_2} - 2\text{pH} - 2\text{pe} - \log a_{H_2O},$$  \hspace{1cm} (3)

where pH $= -\log a_{H^+}$ and pe $= -\log a_e$. Eq. (3) was combined with pH 7 and values of log$f_{O_2}$ and log$a_{H_2O}$ from the MaximAct model to calculate pe, which was then converted to Eh using

$$Eh = \frac{2.303RT\text{pe}}{F},$$  \hspace{1cm} (4)

where $R$, $T$, and $F$ are the gas constant, temperature in Kelvin, and Faraday constant. Note that virtual Eh is increased by either increasing log$f_{O_2}$ or decreasing log$a_{H_2O}$.

Figure 5d shows virtual Eh for the target proteins calculated using Eqs. (3–4) at 25°C, 1 bar, and pH 7. Compared to that of log$f_{O_2}$, the entire Eh profile is tilted up, which reflects the decline of log$a_{H_2O}$ for proteins in younger phylostrata. Representative values of redox potential of the glutathione redox couple ($E_{GSH}$) in subcellular compartments, whole cell lysates, and human blood plasma are shown for comparison (Jones and Sies 2015; Schwarzländer et al. 2016). $E_{GSH}$ values for whole cell lysates reflect contributions from more reducing compartments including the cytosol and mitochondria and more oxidizing compartments including the endoplasmic reticulum (ER) and vacuole (Schwarzländer et al. 2016). The PS 1–11 hump begins and ends close to the $E_{GSH}$ of cell lysates and maximizes near the $E_{GSH}$ of the ER. Between PS 11 and 15 there is a rapid rise toward
$E_{\text{GSH}}$ values characteristic of blood plasma, followed by a return in PS 16 to a value close to $E_{\text{GSH}}$ of the ER.

Figure 5e and f shows the results of the MaximAct analysis applied to target proteins for the consensus gene ages of Liebeskind et al. (2016b). The first four gene ages correspond to the emergence of cellular organisms (GA 1), the last common ancestor of Eukaryota and Archaea (GA 2; Euk_Archaea), genes that are present only in Eukaryotes and Bacteria, representing the horizontal transfer of genes to Eukaryotes (GA 3; Euk+Bac), and Eukaryota (GA 4). There is an increase of both $n_{\text{H}_2\text{O}}$ and $\log_{\text{H}_2\text{O}}$ between GA 1 and 2, and these values are higher than those for all later gene ages. The target proteins for later gene ages are relatively stable near $\log_{\text{H}_2\text{O}} = 0$ and are characterized by virtual $E_h$ values that are higher than $E_{\text{GSH}}$ of whole cell lysates (Fig. 5f).

**Sensitivity of Thermodynamic Parameters to Proteomic Background**

It was argued above that the background proteome should reflect the complete range of biological amino acid composition. However, it might also be prudent to select the background proteins from the genome of the particular organism that is being studied. To examine these effects, Fig. 6a shows the chemical metrics for the proteomes of organisms considered in this study ($H. \text{sapiens, B. subtilis, and D. melanogaster}$). Overlaid on this figure are the chemical metrics for target proteins for phylostrata and biofilm and fly development. The developmental proteomic datasets are analyzed separately below. Because the background proteins are individual protein sequences from a particular genome, while the target proteins have the mean amino acid compositions of groups of proteins identified in distinct phylostratigraphic and proteomic datasets, the target proteins occupy a much smaller region of compositional space than the background.

**Fig. 6** Chemical metrics and thermodynamic parameters calculated using different background proteomes. a Chemical metrics calculated for all protein sequences in different background proteomes and for target proteins described in the text; the latter are indicated by differently colored symbols. The human background proteome was obtained as described in the text; other sources of proteomic data and interpretation of the smooth scatter plots are described in Fig. 1. This plot shows that the compositional range of all the target proteins for different datasets analyzed in this study is much smaller than that of the background proteomes; the differences between sets of target proteins are not analyzed here. b Thermodynamic parameters for target proteins for 16 phylostratigraphic age groups (based on Trigos et al. 2017) calculated using the MaximAct model with different background proteomes. For all other figures in this paper, the background proteome was obtained from the same organism as the source of target proteins.
proteins. Therefore, the presence of background proteins in equilibrium calculations has a buffering effect that keeps the target proteins away from the edges of stability diagrams like that in Fig. 4b. Introducing a set of background proteins in relative stability calculations is a novel way of representing the internal milieu of cells, which is tightly regulated and has a restricted range of chemical properties compared to the exterior (Smith and Morowitz 2016).

Figure 6b shows how changing the background proteome for a single set of target proteins affects the thermodynamic parameters calculated with the MaximAct model. For instance, note that the B. subtilis proteome has a somewhat lower median carbon oxidation state and higher median stochiometric hydration state compared to the human proteome (Fig. 6a). Because of the greater number of high-\(n_{\text{H}_2\text{O}}\) proteins in the genome of B. subtilis, it provides background proteins that are relatively stable in the high-log\(n_{\text{H}_2\text{O}}\) region of chemical potential space, which pushes the maximum activities of the target proteins to lower log\(n_{\text{H}_2\text{O}}\) values (Fig. 6b). Likewise, the relatively low oxidation state of the B. subtilis proteome pushes the maximum activities of the target proteins to higher log\(f_{\text{O}_2}\) values.

Changing the background proteome affects the specific values of thermodynamic parameters but does not greatly affect the qualitative trends within a given dataset (Fig. 6b). For all other calculations in this study, the organism used for the background proteome was selected to be the same as that of target proteins. In future studies that may aim to assess the relative stabilities of target proteins among different organisms, a generic background proteome should be devised that is representative of the total range of biological amino acid composition and that would also be applicable to other domains of life.

### Chemical and Thermodynamic Analysis of Biofilm Development

In a transcriptomic and proteomic study of the development of Bacillus subtilis biofilms, Futo et al. (2021) described three periods of biofilm growth: early (6 h to 1 day), mid (3 to 7 days), and late (1 to 2 months). Time points of 2 days and 14 days were regarded as transitional stages between these periods. In the early period of development, there is a decline in the mean protein length (Fig. 7a). This was computed by combining the lengths of canonical protein sequences from the UniProt database with normalized gene or protein expression values reported by Futo et al. (2021); no phylostrata assignments were used for this or any of the following calculations. The late period of biofilm development, for which only transcriptomic data are available, shows another drop in mean length of the corresponding proteins.

The chemical metrics for individual proteins at each time point were used to compute abundance-weighted mean values of \(Z_C\) and \(n_{\text{H}_2\text{O}}\). After remaining nearly constant in the early period, the mean \(n_{\text{H}_2\text{O}}\) of the proteome-based sequences declines in the first transition and mid-developmental period (2 to 7 days) (Fig. 7b). The time course for the transcriptome-based abundances exhibits fluctuating \(n_{\text{H}_2\text{O}}\) of proteins during this time, followed by a steady drop from 7 days to 2 months. Unfortunately, proteomic data for the late developmental period are not available for comparison. Through early and mid-development there is relatively little variation in mean \(Z_C\) of either the proteome or proteins coded by the transcriptome, but the latter become much more oxidized in the late period (Fig. 7c).

To calculate thermodynamic parameters, amino acid compositions of target proteins were calculated as the abundance-weighted means for sequences inferred from transcriptomes and proteomes. The declining trend of \(n_{\text{H}_2\text{O}}\) is reflected in values of log\(a_{\text{H}_2\text{O}}\) computed from the MaximAct thermodynamic model, which are positive at all but the last time point (Fig. 7d). This can be interpreted as a signal of relatively high hydration potential during the early growth period, followed by proteomic abundances that are closer to metastable equilibrium with each other in an aqueous growth medium. The ambient \(a_{\text{H}_2\text{O}}\) is likely to be not far from unity, as it has been shown that the activity of \(\text{H}_2\text{O}\) in agar medium is very close to that of the solution used to prepare the medium (Gervais et al. 1988).

Optimal values of log\(a_{\text{H}_2\text{O}}\) were combined with those of log\(f_{\text{O}_2}\) (Fig. 7e) to compute virtual \(Eh\) using Eqs. (3–4). The virtual redox potential rises through development, especially in the last period (Fig. 7f). Even if water activity is set to unity instead of taken from the MaximAct model, the sharp rise in \(Z_C\) for the transcriptome-inferred proteins is associated with a predicted increase in virtual \(Eh\). Notably, the formation of wrinkles in biofilms has been postulated to enhance oxygen uptake (Okegbe et al. 2014), and wrinkling in E. coli biofilms has been experimentally associated with greater oxygen penetration than that into the flat base of the biofilm (Hartmann et al. 2021). The carbon oxidation state of transcriptome-inferred proteins rises in 1- to 2-month-old B. subtilis biofilms, well after the appearance of wrinkles around day 3 noted by Futo et al. (2021). This suggests a delay between wrinkling and the putative transcriptional adjustment to oxidizing conditions within the biofilm. Proteomic and oxygen microelectrode or other redox measurements should be obtained at all growth stages in the same biofilms to enable a direct comparison between this model and experiments.
Hydration Dynamics in Development of Fruit Flies

The fruit fly, *Drosophila melanogaster*, is a well-studied invertebrate model organism in genetics and developmental biology. The changes of whole-organism water content and other biochemical constituents during the development of *D. melanogaster* from larvae to adults, when grown on chemically defined axenic medium, were reported by Church and Robertson (1966). As larvae progress through different instars (i.e., a few days post-hatching), the water content first rises to >80%, then varies between about 75 to 80%. The water content decreases suddenly to 66% in the prepupal stage followed by a small rise in adults (Fig. 8a).

Casas-Vila et al. (2017) reported proteomic data for developmental stages of *D. melanogaster*, including embryogenesis, larvae, pupae, and adults. The mean stoichiometric hydration state of proteins from the fly developmental proteome is plotted in Fig. 8b. \( n_{H_2O} \) is almost constant during embryogenesis and three instars of larvae (L1, L2, L3), then drops abruptly in stage L3c (L3 crawling larva). The pupae collected on different days (P1 to P5) exhibit a somewhat higher and variable \( n_{H_2O} \), which is still lower than the embryos. Finally, \( n_{H_2O} \) increases in young adults and then again in old adults, which have \( n_{H_2O} \) values somewhat less than those of embryos and early larvae.

Remarkably, the stoichiometric hydration state of proteins drops precipitously when the crawling larvae leave the medium, at the same time as a sharp drop in organismal water content (Church and Robertson 1966). Later, a higher organismal water content in adult flies compared to pupae is reflected in rising proteomic \( n_{H_2O} \) for adults. Water activity computed from the MaximAct analysis, in which the target proteins were modeled as having the mean amino acid compositions for growth stages weighted by abundances of transcripts or proteins: d and e Optimal values of \( \log_{aH_2O} \) and \( \log fO_2 \), i.e., those that maximize the metastable equilibrium activities of the target proteins against the background proteome for *B. subtilis*. Thermodynamic parameters are mean values for 100 runs, each consisting of 2000 randomly selected background proteins. f Virtual redox potential (\( Eh \)) computed from Eqs. (3–4) and the optimal values of \( \log_{aH_2O} \) and \( \log fO_2 \). Dashed lines indicate \( Eh \) values calculated for the same \( \log fO_2 \) values and unit activity of \( H_2O \).
Fig. 8 a Organismal water content during growth of fruit flies (D. melanogaster) from larvae (hours after hatching) to pupal and adult stages, replotted from Church and Robertson (1966, their Fig. 4). b Mean stoichiometric hydration state of proteins computed from the developmental proteome of Casas-Vila et al. (2017). The shaded area represents the bootstrap confidence intervals. Labels starting with “E,” “L,” and “P” refer to embryogenesis, larval, and pupal stages. “Ay” and “A” stand for young adults and adults, and “f” and “m” indicate female and male adults. c Values of log$_{H_2O}$ that maximize the activities of target proteins for each developmental time point against the D. melanogaster proteomic background. Horizontal lines represent values computed for the differentially expressed proteins in embryos and adults using data from a different study (Fabre et al. 2019). d Values of Z$_C$ and n$_{H_2O}$ computed for differentially expressed proteins in embryo and adult flies (Fabre et al. 2019). The plots were made using R’s boxplot() function; the bottom and top of the boxes correspond to the first and third quartile, the notch (thick bar) indicates the median, and the whiskers are drawn at a data point that is no more than 1.5 times the height of the box away from the box. Individual points beyond the whiskers are plotted. p values were calculated using the two-sided Wilcoxon rank-sum test. e Median values of n$_{H_2O}$ and Z$_C$ from the plots in (d) and median values of optimal log$_{H_2O}$ and virtual Eh for the same groups of differentially expressed proteins. Filled and open symbols indicate virtual Eh calculated from the optimal values of log$_{H_2O}$ and log$_{H_2O}$ and for unit activity of H$_2$O, respectively.

Analysis of proteomic data from a different study (Fabre et al. 2019) shows significantly higher stoichiometric hydration state of proteins enriched in embryos compared to adults, in contrast to nearly indistinguishable mean values of carbon oxidation state (Fig. 8d). For this dataset, only binary classification of differentially expressed proteins was used, and the MaximAct analysis was performed for each differentially expressed protein rather than for mean amino acid compositions. Although the precise age of the adult flies was not given by Fabre et al. (2019), their description refers to the emergence of adults less than 9 days after egg laying. Considering the number of days spent in larval and pupal growth, this suggests an age closer to the young adults (4 hours after eclosure) than the old adults (1 week-old flies) studied by Casas-Vila et al. (2017). Accordingly, the developmental proteome of Casas-Vila et al. (2017) and differentially expressed proteins of Fabre et al. (2019) both exhibit considerably higher theoretical water activity in embryos than in young adults (Fig. 8c, e).

Despite the small difference in Z$_C$ between groups of proteins with higher expression in embryos or adults, virtual Eh derived from the MaximAct analysis is higher in adults (Fig. 8f). This occurs because log$_{H_2O}$ and pe have the same sign in Eq. (3), so higher log$_{H_2O}$ corresponds to lower pe and Eh at constant log$_{H_2O}$; if water activity is fixed at unity, then the difference in virtual Eh vanishes (open symbols in Fig. 8f). In vivo measurements using roGFP2 fusion proteins reveal pro-oxidative changes in...
aging flies (Albrecht et al. 2011) that support the physiological relevance of the predicted rise in virtual \(E_h\).

Discussion

Carbon Oxidation State and Redox Potential

In a first approximation, carbon oxidation state of biomolecules can be predicted to increase as an energy-minimizing response to higher environmental \(O_2\) concentration or intracellular redox potential, depending on the scale of the system under consideration, but thermodynamic models provide a more theoretically grounded prediction of protein (or proteomic) transformations in changing redox conditions. It is tempting to speculate that the initial rise of \(Z_C\) of proteins that appeared after the origin of the first cells (Fig. 2b) might be a geobiological record of the oxygenation of Earth’s atmosphere and oceans. The last universal common ancestor (LUCA) was most likely an anaerobic chemoautotroph that inhabited reducing hydrothermal environments (Weiss et al. 2016), so it comes as little surprise that the oldest gene ages in Fig. 3a and b correspond to proteins with relatively low carbon oxidation state. The next oldest age group in Fig. 3b is for Pfam domains that emerged after LUCA but before the emergence of eukaryotes from Bacteria and Archaea (as described by James et al. 2021; see also Weiss et al. 2016, their Figure 1). The boxplots in Fig. 3b are consistent with rising \(Z_C\) between protein domains conserved in LUCA and the pre-eukaryotic ancestors. Additional work is needed to confirm whether these trends inferred from amino acid compositions of proteins in extant eukaryotes are also present in the archaeal and bacterial domains.

Compared to transmembrane domains that likely evolved in a hydrophobic environment, non-transmembrane (cytosolic) domains have a higher \(Z_C\) and exhibit a larger and more significant increase of \(Z_C\) across phylostrata (Fig. 3b). A low \(Z_C\) of membrane-associated proteins can be expected based on their high content of hydrophobic amino acids (Dick 2014). The relatively flat trend for transmembrane domains suggests a smaller evolutionary variability in their elemental composition compared to cytosolic proteins. The findings for cytoplasmic proteins in particular are compatible with a chemical link between the oxygenation of Earth’s atmosphere and the carbon oxidation state of proteins. This geobiological model should be considered as being complementary to interpretations based on biophysical metrics that are also linked to the amino acid compositions of proteins (e.g., hydrophobicity and intrinsic structural disorder; James et al. 2021).

Following from the chemical analysis, a thermodynamic model allows predicting the virtual redox potentials (\(E_h\)) that stabilize target proteins for phylostratigraphic age groups. The Euk_Archaea group is of particular interest because it represents the last common ancestor of Eukaryotes and Archaea. Although proteins coded by genes in the Euk_Archaea group are slightly more oxidized than those of cellular organisms (Fig. 2b), their maximum activity occurs at higher \(\log_{H_2O}\). It follows from Eqs. (3–4) that the Euk_Archaea proteins are stabilized by a lower virtual redox potential, close to −300 mV (Fig. 5f). Notably, such a low virtual redox potential is not possible if the activity of \(H_2O\) is assumed to be unity (dashed line in Fig. 5f). This low virtual redox potential is consistent with the views of the reductive overall cellular physiology, typical of archaeal cells, that operated before the endosymbiotic transfer of mitochondria (Martin and Sousa 2016), and of the reducing cytosolic \(E_GSH\) of modern cells as a remnant of redox conditions in the primordial environment (Schwarzländer et al. 2016). The subsequent innovation of oxidative chemistry in aerobes (Williams and Fraústo Da Silva 2003) is a plausible explanation for the rise in virtual \(E_h\) at GA 3 to 5. Further support for this thermodynamic characterization requires analysis of phylostratigraphic data for other lineages, which is not done here.

Although oxygen is required for complex animal life, oxygen concentrations decline rapidly within multicellular structures if the supply is by diffusion alone. The effect of such oxygen gradients on carbon oxidation state of proteins is apparent in laboratory experiments: cells grown in 3D cell culture, whose interiors are characterized by hypoxic conditions, express proteins with lower \(Z_C\) than do cells grown in monolayers (Dick 2021). Therefore, a plausible hypothesis is that the beginning of a negative shift in \(Z_C\) around the emergence of Eumetazoa (Figs. 2, 3a) reflects oxygen gradients in early multicellular structures. The continued drop in subsequent phylostrata might result from hypoxic microniches (for example, those that sustain stem cells) even as circulatory systems became more advanced. Although speculative at the moment, this type of reasoning centered on oxidation–reduction conditions might one day lead to deeper links between protein evolution and cell physiology.

Stoichiometric Hydration State and Water Activity

Through analysis of stoichiometric hydration state, it is apparent that protein expression at the proteome scale may be chemically coupled to water content in developing organisms. Specifically, for Drosophila melanogaster, the large decrease in proteomic \(n_{H_2O}\) at the crawling larva stage (L3c) is aligned with the measured prepupal decrease in organismal water content (Church and Robertson 1966). Stoichiometric hydration state of proteins also decreases during growth of Bacillus subtilis biofilms, but no experimental reports of measured water content could be found for
Hydration dynamics of developing biofilms might exhibit similarities with that of animals, for which a large body of work documents decreasing water content through early developmental stages (Logan and Himwich 1972; Calcagno et al. 1972; Friis-Hansen 1983). Together with the relatively high $\gamma_H^O$ of proteins in the earliest phylostratigraphic age groups, these results can be used to postulate that elevated hydration potential is a key factor in the maintenance of protein expression patterns that are characteristic of both embryos and unicellular organisms.

Thermodynamic models in geochemistry often involve one or more “perfectly mobile components,” which are represented by their chemical potentials, instead of by bulk composition (Rumble 1982; Evans et al. 2013). Oxygen fugacity is one such descriptive variable in many geochemical models, while water activity is often considered to remain close to unity except for certain systems such as brines (Helgeson 1968). In contrast, in this study the chemical potentials of both $O_2$ and $H_2O$ were used as independent variables in order to explore the landscape of relative protein stabilities in two dimensions. The theoretical $a_{H_2O}$ reaches much lower values than measurements in saturated salt solutions (e.g., saturation of NaCl corresponds to 0.755 water activity; Stevenson et al. 2015). At the other extreme, the theoretical values can be greater than unity. This represents an unphysical condition as pure water has unit activity. It may be possible to obtain $a_{H_2O} > 1$ in molecular dynamics simulations of mixtures of $H_2O$ and organic media due to oversaturation of $H_2O$ and cluster formation in a non-polar solvent, but those results were regarded as anomalous by the investigators (Wedberg et al. 2012).

By analogy with the situation for oxygen fugacity in petrology, where vanishingly low values have no physical meaning as partial pressure but remain useful as indicators of oxidation potential (Frost 1991), water activity predicted from metastable equilibrium calculations for proteins must be interpreted as a theoretical indicator of hydration potential that may not coincide with experimental measurements. Despite this, it is noteworthy that the thermodynamic analysis yields theoretical values of $a_{H_2O}$ that approach unity for later phylostratigraphic age groups and for advanced stages of biofilm development (Figs. 5e, 7d). An exception seems to be stages of fly development, which appear to be poised at higher water activity (Fig. 8c). This could be in part a consequence of higher $a_{H_2O}$ predicted by using the background proteome from Drosophila compared to those from other organisms. A productive line of inquiry would be to find a universal set of background proteins with the property that thermodynamic models for various evolutionary and developmental datasets overlap with unit water activity, that is, a physically realistic condition.

In summary, when analyzed using thermodynamic methods adapted from geochemistry, differences in amino acid compositions and abundances of proteins reflect a water-dominated but dynamic hydration state of cells. Besides its importance for polymerization reactions in prebiotic conditions and for macromolecular crowding and phase separation in living cells (Bagatolli and Stock 2021), water activity can therefore be regarded as a fundamental thermodynamic parameter for organismal development and Darwinian evolution.

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Data Availability Data were obtained from the UniProt database (The UniProt Consortium 2019) and the supporting files of previous studies (Liebeskind et al. 2016b; Casas-Vila et al. 2017; Trigos et al. 2017; Fabre et al. 2019; Futo et al. 2021; James et al. 2021) as described in the Materials and Methods and figure captions. Files with phylostrata assignments and UniProt IDs are available in the R package canprot version 1.1.2 (Dick 2021). Processed data files used in this study are in the “extdata/evdevH2O” directory of the JMDplots package (version 1.2.12 deposited on Zenodo with accession number 6137783) (Dick 2022), except for the differential expression dataset of Fabre et al. (2019), which is located under “extdata/evdevH2O/RMDplot.”

Declarations

Conflict of interest The author declares no competing interests.

Code Availability The code used to make the figures for this paper is available in the JMDplots package (Dick 2022). The maximum activity analysis described here has been implemented in a new function named MaximAct(). The “evdevH2O.Rmd” vignette in the package runs the functions to make each of the figures and has code blocks to generate particular values mentioned in the text.

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