Stabilization of highly polar BiFeO$_3$-like structure: a new interface design route for enhanced ferroelectricity in artificial perovskite superlattices

Hongwei Wang$^1$, Jianguo Wen$^{2, *}$, Dean J. Miller$^2$, Qibin Zhou$^4$, Mohan Chen$^3$, Ho Nyung Lee$^3$, Karin M. Rabe$^4$, and Xifan Wu$^1, *$

$^1$Department of Physics, Temple University, Philadelphia, PA 19122, USA
$^2$Center for Nanoscale Materials, Argonne National Laboratory, Argonne, IL 60439, USA
$^3$Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
$^4$Department of Physics and Astronomy, Rutgers University, Piscataway, NJ 08854-8019, USA and
$^5$Department of Mechanical and Aerospace Engineering, Princeton University, Princeton, New Jersey 08544, USA

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In ABO$_3$ perovskites, oxygen octahedron rotations are common structural distortions that can promote large ferroelectricity in BiFeO$_3$ with an R$_3c$ structure $^1$, but suppress ferroelectricity in CaTiO$_3$ with a Pbnm symmetry $^2$. For many CaTiO$_3$-like perovskites, the BiFeO$_3$ structure is a metastable phase. Here, we report the stabilization of the highly-polar BiFeO$_3$-like phase of CaTiO$_3$ in a BaTiO$_3$/CaTiO$_3$ superlattice grown on a SrTiO$_3$ substrate. The stabilization is realized by a reconstruction of oxygen octahedron rotations at the interface from the pattern of nonpolar bulk CaTiO$_3$ to a different pattern that is characteristic of a BiFeO$_3$ phase. The reconstruction is interpreted through a combination of amplitude-contrast sub 0.1nm high-resolution transmission electron microscopy and first-principles theories of the structure, energetics, and polarization of the superlattice and its constituents. We further predict a number of new artificial ferroelectric materials demonstrating that nonpolar perovskites can be turned into ferroelectrics via this interface mechanism. Therefore, a large number of perovskites with the CaTiO$_3$ structure type, which include many magnetic representatives, are now good candidates as novel highly-polar multiferroic materials $^3$.

INTRODUCTION

New mechanisms to generate ferroelectricity (FE) have recently been the subject of active research, due to both fundamental interest and the technological importance of ferroelectrics and related materials $^4$. Novel ferroelectrics have potentially higher performance for practical applications, as well as potential compatibility with other functional properties such as magnetism, yielding multiferroics and other multifunctional materials $^5$ $^6$ $^7$ $^8$ $^9$ $^10$.

Artificially structured perovskite superlattices offer rich opportunities for novel ferroelectricity $^7$ $^11$. Nonbulk phases for the constituent layers can be stabilized by the mechanical and electrical boundary conditions characteristic of a superlattice $^12$ $^13$, potentially turning constituents that are nonpolar in bulk form into ferroelectrics $^14$ $^15$. Competing low-energy metastable phases can be readily found in perovskites with low tolerance factors, promoting oxygen octahedron rotation (OOR) instabilities along the Brillouin-zone-boundary R-M line. The ground state structure in such cases is generally the nonpolar orthorhombic Pbnm structure. As a typical example, the oxygen octahedron in a CaTiO$_3$ (CTO) can be described by its rotation around [110] axis and an in-phase rotation around [001] axis (a$^+$$^-$$^-a^-$ in Glazer notation). Such a pattern of OOR favors antipolar behavior instead of FE $^2$. On the other hand, OOR with a different pattern can also promote large FE. As one famous example, in BiFeO$_3$ (BFO) with R$_3c$ structure, the oxygen octahedron can be characterized by a rotation around [110] and an out-of-phase rotation around [001], yielding a fairly large polarization along [111] (a$^-a^-a^-$ in Glazer notation). Compared to the widespread of CTO-like materials, BFO-like perovskites are relatively rarely seen. As a result, the OOR is generally thought to suppress FE in perovskites.

However, for many perovskites, the BFO-like structure serves as a low-energy metastable phase $^2$. Therefore, it would be beneficial if an artificial perovskite superlattice could stabilize this metastable phase for the entire constituent layers or in a region near interface. To this end, a reliable design mechanism can be derived only from precisely determined atomic positions in experiments followed by theoretical interpretations based on first-principles calculations.

EXPERIMENTAL AND FIRST-PRINCIPLES RESULTS

Aberration-corrected high-resolution transmission electron microscopy (HRTEM) is a powerful method for accurate visualization of oxygen octahedron distortions $^16$ $^17$. Recently, it was shown that amplitude contrast imaging in HRTEM could be used to discriminate heavy and light element columns based on channeling contrast $^18$, allowing one to locate the exact interface and to visualize OOR angles in different atomic layers (see Supplementary Materials S1). Fig. 1(a) shows an experimental HRTEM image of a 4BaTiO$_3$(BTO)/4CTO superlattice film along the [110] direction of the SrTiO$_3$ (STO) substrate. This
FIG. 1: Experimental and simulated HRTEM images showing oxygen octahedral tilts in the 4BTO/4CTO superlattice film grown on a STO substrate along [110].
(a). Experimental HRTEM image using an amplitude contrast imaging method ($Cs = 3\, \mu m$, $Cc = 1\, \mu m$, $\Delta f = -1\, nm$). BaO columns (dark dots) and CaO columns (bright dots) show different channeling contrast. Oxygen atomic columns displace differently, either upward or downward, with respect to the central Ti atoms in box 1, 2 and 3. 0.14\,nm indicates the spacing between Ti and O columns. Accumulated electron dose is $3 \times 10^4$ electrons/\,nm$^2$. (b). Simulated HRTEM image using the atomic positions obtained from first-principles calculations. The simulated image matches well with the experimental image except a sharper column contrast in the simulated image compared to the experiment one because electron beam induced object excitations are omitted as pointed out by Kisielowski et al. (see Supplementary Materials S4).

image was obtained by correcting both spherical and chromatic aberrations to achieve amplitude contrast imaging conditions ($Cs = 3\, \mu m$, $Cc = 1\, \mu m$). In this image, channeling contrast between Ca and Ba columns is clearly observed: atomic columns of CaO and BaO appear as bright and dark dots, respectively; oxygen and Ti columns appear as bright dots. Due to the interdiffusion of Ba and Ca at the interface, the intensity at A site varies depending on the ratio of Ca and Ba as discussed in detail in the supplementary material (S2). It is seen that BTO and CTO grow coherently on the STO substrate, showing the same in-plane lattice constant as that of STO, and elongated c-axis in the BTO layer and shortened c-axis in the CTO layer (see Supplementary Materials S3). Within the CTO layer of the superlattice (box 1), a strongly corrugated TiO$_2$ plane is observed in which the oxygen atoms displace upward and downward with respect to the central Ti atoms, corresponding to an OOR around [110] by 9°, comparable to that of bulk CTO. For TiO$_2$ planes between two BaO planes (box 3), alternating displacement of the oxygen atoms, and thus the amplitude of the OOR, is negligible, consistent with the fact that bulk BTO strongly resists OORs. For TiO$_2$ planes between one BaO and one CaO plane (box 2), the OOR around [110] is 3°, smaller than that in the interior of the CTO layers.

For comparison, in Fig. 1(b) we present the simulated HRTEM image using the atomic positions of the 4BTO/4CTO superlattice obtained from first-principles calculations. The simulated HRTEM image for the computed structure shows the same pattern of OOR as in the experiment (compare boxes 1, 2, and 3 in Fig. 1(a) and (b)), with amplitudes of 12.5° in the CTO layer and 5.5° at the interface. The quantitative difference in OOR around [110] angles from the experimental observation can be partly attributed to the fact that the experiments were performed at $T = 300$ K, while the ground state structural relaxation by density functional theory was at $T = 0$ K. In addition, in this image it is possible to discern the small uniform displacement of the oxygens relative to the Ti atoms in the TiO$_2$ plane, which is associated with the spontaneous polarization of the superlattice. While this displacement is present in all the TiO$_2$ layers, it can be more easily identified in those belonging to the interior BTO layers, which do not have the corrugation associated with OOR.

We use the atomic-scale information from the first-principles results for a detailed layer-by-layer investigation of the properties of the superlattice. We focus our discussion on the 6BTO/6CTO superlattice, which allows a clearer distinction between the interface and interior layers; the corresponding results for the 4BTO/4CTO superlattice are similar (see Supplementary Materials S6). The computed spontaneous polarization is 29 $\mu C/cm^2$ along [001] and 11 $\mu C/cm^2$ along [110]. The resulting layer-by-layer decomposed structural distortions and polarizations are shown in Fig. 2.

TABLE I: Computed bulk properties of R$_3^1$($c$), R$_3^2$($c$), R$_3^3$($c$).

| Boundary Condition | Fixed E field | Fixed D field |
|--------------------|---------------|---------------|
| E = 0 V/m          | $D = 29 \, \mu C/cm^2$ |
|                     | $P_{00i}$     | $P_{110}$     |
| Symmetry           | P$4mm$        | P$6mm$        | e-R3c | P$6mm$        | e-R3c |
| R$_x$              | 0             | 7.7           | 0     | 7.6           | 0     |
| R$_y$              | 0             | 0             | 7.3   | 0             | 7.2   |
| R$_{xy}$           | 0             | 12.7          | 11.5  | 12.8          | 11.7  |
| ADIS               | 0             | 0.29          | 0     | 0.32          | 0     |
| $P_{00i}$          | 41.93         | 0             | 20.01 | 27.81         | 28.96 |
| $P_{110}$          | 0             | 26.40         | 52.19 | 24.53         | 51.25 |
| $P_{01}$           | 41.93         | 26.40         | 55.89 | 37.08         | 58.87 |
| c/a                | 1.067         | 0.964         | 0.968 | 0.965         | 0.967 |
| Energy             | -162.645      | -164.158      | -164.066 | -164.106      | -164.040 |
FIG. 2: Computed local properties associated with ferroelectric and non-polar modes in 6BTO/6CTO superlattice and schematic plots for the atomic displacements of the oxygen octahedron rotation and ferroelectric modes. First-principles calculations of 6BTO/6CTO superlattice showing layer-by-layer decompositions in-phase oxygen octahedron rotation around [001] \( R_{ij} \), out-of-phase oxygen octahedron rotation around [001] \( R_{ij}^{\alpha} \), in-plane polarization \( P_{110} \), out-of-plane polarization \( P_{001} \), antipolar modes (AFE) represented by A-site cation displacements (ADIS), and oxygen octahedron rotation around [110] \( R_{xy} \). The corresponding strained bulk values are also denoted by the open symbol in the plot, and in particular, the open strained bulk values in \( P_{001} \) are predicted by the dielectric slab model \[14\]. A highly polar BiFeO\(_3\)-like interface phase in CTO is highlighted in blue.

be closely related to those of strained bulk materials under the electrical boundary condition of a fixed displacement (\( D \)) field, imposed by the superlattice as summarized in Table I. Indeed, as shown in Fig. 2, the interior BTO layers have negligible OOR with a polarization of 32 \( \mu C/cm^2 \) along the [001] direction. This is consistent with the structure and large polarization of strained BTO; the reduction from the strained bulk value of 42 \( \mu C/cm^2 \) can be attributed to the electrostatic cost of polarizing the nonpolar CTO layer. Both bulk CTO and strained bulk CTO are characterized by the strong OORs due to structural instabilities at the zone-boundary \( M \) and \( R \) points. Therefore, the interior CTO layers are dominated by \( R_{xy} \) and \( R_{ij}^{\alpha} \), which are OOR around [110] and an in-phase OOR around [001] respectively as shown in Fig. 2. In addition, a large antipolar (AFE) mode develops in the CTO layers that can be clearly identified by the zig-zag movement of A-site displacement along [110] direction. It should be stressed that this antipolar distortion is a structural distortion at the X point favored by the trilinear coupling due to the pattern of OOR in CTO-like materials. The above distortion in the interior CTO layers can be clearly seen in Fig. 2 as well as in the TEM image in Fig. 1 (a) (see Supplementary Materials S5). This AFE mode was also recently pointed out to be the key to the suppressed FE in all CTO-like perovskites \[2\]. Due to the applied tensile epitaxial strain, the interior CTO layers are polar along [110] direction with a magnitude of 26.4 \( \mu C/cm^2 \) just like the strained CTO \[20\].

If the interface effect is negligible, the dielectric slab model can be used to predict the polarization, yielding a value of 22.4 \( \mu C/cm^2 \) along the [001] direction. The first-principles calculation gives \( P_{001} = 29.0 \mu C/cm^2 \). The discrepancy from the dielectric slab model suggests that the interface effect cannot be neglected. Such a large enhancement of the polarization (~ 25%) is a strong indication of a highly polar interface reconstruction. Indeed, examination of Fig. 2 reveals that the structure at the interface of the CTO layers differs significantly from that of the strained bulk CTO, with the OOR being suppressed at the interface of the superlattice. The AFE type displacement, which is driven by the trilinear coupling involving the OORs of CTO, is suppressed too. Furthermore, a new structural pattern of OOR emerges at the interface: an OOR around the [110] axis and an out-of-phase OOR around the [001] axis for a TiO\(_6\) sandwiched...
between two interface CaO layers, with rotation angles comparable to those of the strained bulk in-phase OOR. This new structure pattern is exactly the same as one would observe for oxygen octahedron rotation in BiFeO$_3$ and similar perovskites with R3c symmetry.

**MICROSCOPIC MECHANISM**

Here, we propose that this change in structure at the interface can be interpreted as the local stabilization of a BFO-like structure different from that of the bulk CTO. As far as the topology of the oxygen octahedron rotation network is concerned, oxygen octahedra in both BFO and CTO rotate around [110]; however, BFO differentiates itself from CTO by its out-of-phase OOR around [001] instead of the in-phase counterpart in CTO. The out-of-phase and in-phase OOR around [001] originate from symmetry-nonequivalent structural instabilities at the R and M points respectively. This stabilization of a BFO-like structure in CTO layers near the interface is derived from the metastable polar e-R3c phase and is compatible with a much larger polarization than that in bulk CTO as shown in Table I. It has been shown that this phase cannot be stabilized relative to the Pbnm phase by epitaxial strain alone [21]. However, in the superlattice, the suppression of the tilt angles by proximity to BTO, assisted by the electrical and mechanical boundary conditions that favor a phase with a component of polarization along [001], is sufficient to stabilize the structure [22].

To explore the stabilization of this phase more quantitatively, we constructed first-principles based models for the strained Pbnm phase (designated $E$-CTO$''$(R$_z^i$, R$_xy$, AFE$_{xy}$, FE$_{xy}$)) and for the metastable e-R3c phase ($E$-BFO$''$(R$_z^o$, R$_xy$, FE$_{xy}$, FE$_z$)). Facilitated by space group symmetry analysis, the models of both $E$-CTO$''$ and $E$-BFO$''$ are built through polynomial expansions of the total energy from first-principles calculations with respect to the high-symmetry reference structure (P4/mmm phase) in terms of the amplitudes of the relevant modes. In the above, R$_z^i$, R$_z^o$, R$_xy$, AFE$_{xy}$, FE$_{xy}$, FE$_z$ represent the mode amplitude of in-phase OOR around [001], out-of-phase OOR around [001], OOR around [110], in-plane antipolar mode and in-plane and out-of-plane FE modes respectively. The resulting models are shown in the following for $E$-CTO$''$ and $E$-BFO$''$, respectively as (see Supplementary Material 7 for fitted coefficients):

$$
E_{-CTO''} = a_1 R_z^2 + b_1 R_z^4 + a_2 R_z^2 + b_2 R_{xy}^2 + a_3 AFE_{xy}^2 + b_3 AFE_{xy} + a_4 FE_{xy}^2 + b_4 FE_{xy} + c_1 R_{xy}^2 R_z^2 + c_2 R_{xy}^2 AFE_{xy}^2 + c_3 R_{xy}^2 FE_{xy} + c_4 R_{xy}^2 AFE_{xy} + c_5 R_{xy}^2 FE_{xy} + c_6 AFE_{xy}^2 FE_{xy} + d_1 R_z R_{xy} AFE_{xy},
$$

(1)

$$
E_{-BFO''} = a_1 R_z^2 + b_1 R_z^4 + a_2 R_z^2 + b_2 R_{xy}^2 + a_3 AFE_{xy}^2 + b_3 AFE_{xy} + a_4 FE_{xy}^2 + b_4 FE_{xy} + c_1 R_{xy}^2 R_z^2 + c_2 R_{xy}^2 AFE_{xy}^2 + c_3 R_{xy}^2 FE_{xy} + c_4 R_{xy}^2 AFE_{xy} + c_5 R_{xy}^2 FE_{xy} + c_6 AFE_{xy}^2 FE_{xy} + d_1 R_z R_{xy} AFE_{xy},
$$

(2)

Assuming the angles of the oxygen octahedron rotations are tunable parameters under experimental conditions, we further define the functions $F_{-CTO''}(R_z^i, R_{xy}) = \min E_{-CTO''}(R_z^i, R_{xy}, AFE_{xy}, FE_{xy})$, and $F_{-BFO''}(R_z^o, R_{xy}) = \min E_{-BFO''}(R_z^o, R_{xy}, FE_{xy}, FE_z)$. In order to understand how the BFO-like phase can be stabilized relative to the CTO-like phase, we then evaluate $\Delta E = F_{-BFO''} - F_{-CTO''}$ as functions of oxygen octahedron rotation magnitudes around [110] and [001]. The resulting $\Delta E$ is presented in Fig. 3. The total FE mode amplitudes are also presented by the color spectrum in the base plane in Fig. 3. It can be seen that when the angles are fixed to the values of bulk CTO regions in the superlattice, as shown in Fig. 2 (R$_z$ = 8.3$^\circ$ and R$_{xy}$ = 12.6$^\circ$), the CTO-like phase is strongly favored in energy. In the CTO-like phase, as shown in Fig. 2 and Table 1, the antipolar distortion is favored over the FE distortion due to the large trilinear coupling term $\sim R_z R_{xy} AFE_{xy}$ in Eq. 1. Notably, when the amplitudes of OORs are reduced, the BFO-like phase becomes energetically more stable than the CTO-like phase as shown in Fig. 3. This indicates that the BFO-like phase...
can be stabilized over the CTO-like phase when the OOR is reduced. When the above transition takes place, the OOR around [001] will change abruptly from in-phase rotation to out-of-phase rotation signifying a more drastic change in the topology of the oxygen octahedron network, as guided by the yellow plane at \( \Delta E = 0 \) in Fig. 3. In addition to the pattern change of OOR, the BFO-like phase is generally found to have much larger polarization than that in the CITO-like phase as shown by the color spectrum in Fig. 3. The much stronger FE polarization is expected, originating from the e-R3c phase; it can also be easily understood by the large four-linear coupling term \( R^z_{xy} R_{xy} F_{xy} F_{xy} \), which promotes FE in both the in-plane and out-of-plane directions.

This mechanism leads to the BFO-like phase that exists at the interface of the BTO/CTO superlattice. Assuming the octahedra to be fairly rigid, the reduction of OOT is imposed by the adjoining BTO layer, which is strongly resistant to the OOR. A direct consequence of the stabilization of the BFO-like structure at the interface is that the polarization of the superlattice is greatly enhanced. For a particular choice of angles with \( R^z_{xy} = 5.7^\circ \) and \( R_{xy} = 6.6^\circ \) similar to those at the interface of the BTO/CTO superlattice, the computed polarization of the BFO-like phase is over 54.0 \( \mu \text{C/cm}^2 \), which is comparable to the polarization in the bulk e-R3c CTO as shown in Table 1. In the superlattice, the BFO-like phase is further favored by both the electric and mechanical boundary conditions imposed by the polarization of the BTO layer according to Eq. 2. Under the continuous displacement field along [001] direction, the electric boundary condition tends to polarize the CTO components with a larger \( F_{xy} \). Under the tensile strain, the mechanical boundary condition effectively enhances \( F_{xy} \). The larger \( F_{xy} \) and \( F_{xy} \) tend to further lower the energy through \( R^z_{xy} R_{xy} F_{xy} F_{xy} \) and stabilize the BFO-like phase.

### INVERSE DESIGN OF NEW FERROELECTRIC MATERIALS

It has long been recognized that oxygen octahedron rotation can play different roles in perovskites promoting FE in BFO-like materials \( [1, 2] \) but suppressing FE in CTO-like materials \( [24] \). However, the results presented here suggest that a transition between these two phases can be achieved through interface engineering in a superlattice. In addition to improving the fundamental understanding of these transitions, these results suggest a new pathway to induce FE in functional oxide materials.

The enhanced polarization observed in the BTO/CTO superlattice studied here demonstrates this mechanism. To explore the potential of this approach, we predict a few more superlattices \( \text{A'}\text{BO}_3/\text{A''BO}_3 \) as listed in Table II.

| Material | \( P_{sbulk} \) | \( P_{sbulk} \) | \( P_M \) | \( P_{Ct} \) | \( \text{Enh.} \) | \( \text{Sub} \) |
|----------|----------------|----------------|--------|----------|----------|--------|
| \( \text{BaTiO}_3/2\text{CaTiO}_3 \) | 41.9 | 25.7 | 25.9 | 39.9 | 56% | SrTiO_3 |
| \( \text{BaTiO}_3/2\text{CdTiO}_3 \) | 50.8 | 37.8 | 34.2 | 50.4 | 47% | NdGaO_3 |
| \( 2\text{KNbO}_3/2\text{NaNbO}_3 \) | 36.2 | 36.2 | 36.2 | 50.4 | 47% | DyScO_3 |
| \( 2\text{KNbO}_3/2\text{AgNbO}_3 \) | 36.2 | 36.2 | 36.2 | 50.4 | 47% | DyScO_3 |

Within this category of tailored materials, one of the parent bulk \( \text{A'}\text{BO}_3 \) is chosen to be a “CTO-like” perovskite with strong oxygen octahedron rotations, resulting in an antipolar type (\( \text{CaTiO}_3 \) and \( \text{CdTiO}_3 \)) \( [25] \) or an antiferroelectric type (\( \text{AgNbO}_3 \) and \( \text{NaNbO}_3 \)) \( [26, 27] \) ground state that is favored by the trilinear coupling term. The other parent bulk \( \text{A''BO}_3 \) is chosen to have a large tolerance factor resisting oxygen octahedron rotation and a strong FE polarization. Similar to what we have already shown for the BTO/CTO example, the out-of-phase OORs around [001] are induced around the interface layers of \( \text{A'}\text{BO}_3 \) (see Supplementary Materials S8 for examples of \( 2\text{BaTiO}_3/2\text{CaTiO}_3 \) and \( 2\text{KNbO}_3/2\text{AgNbO}_3 \)). As a result, the overall polarizations of the superlattices are enhanced compared to the predictions from the dielectric slab model, which is equivalent to applying the charge continuity principle only and neglecting completely the possible interface reconstruction.

This approach to create new FE materials by interfacial control can also be used to create new materials even where the building blocks could come only from nonpolar perovskites. In Table III we list a few predicted \( \text{A''BO}_3/1\text{A'}\text{BO}_3 \) superlattices within this category. These interface materials also provide us a good opportunity to perform rigorous mode decompositions based on space group theory followed by a careful comparison between the interface materials and the parent bulk compounds. The resulting mode decompositions and the local properties are also shown in Table III. The \( \text{A'}\text{BO}_3 \) is again a “CTO-like” perovskite with strong oxygen octahedron rotations. The above property is clearly represented by the large mode amplitudes of \( Q_{R_{xy}} \) and \( Q_{R^z_{xy}} \) which correspond to an OOR around [110] and in-phase OOR around [001] as shown in Table III. Under such a pattern of OORs, the antipolar mode \( Q_{A'F_{xy}} \) is favored, and FE is strongly suppressed resulting in zero polarization along all directions. On the other hand, \( \text{A''BO}_3 \) is a strong “cubic” perovskite \( [28, 30] \) that does...
TABLE III: Predicted new artificial ferroelectric materials based on non polar perovskites. (1) Mode decompositions (Å) of Q_ε as out-of-phase OOR around [001], Q_R as in-phase OOR around [001], Q_F as OOR around [110], and Q_F as polar distortion along [001], Q_F as polar distortion along [110], and Q_F as in-plane antipolar distortion. Their symmetries are labeled as M^+, M^-, M^', Γ^, and Γ^' respectively; (2) OOR angles (degrees) R^, R^', R^o for out-of-phase OOR around [001], in-phase OOR around [001], and OOR around [110] (octahedron tilt) respectively; (3) The polarizations (µc/cm^2) along [001] direction P_{001}, along [110] direction P_{110}, and the total polarization P_T; (4) The polarization enhancement (Enh.); (5) Substrate for the epitaxial growth of the superlattices, KTaO_3(n=3.99 Å), MgO(a=4.214 Å). (6) Space group symmetry (Sym.) of both strained bulk and superlattice.

| A' (A")BO_3 | Mode Decompositions (Å) | OOR Angles (°) | Polarization (µc/cm^2) | Enh. | Substrate | Sym. |
|--------------|--------------------------|----------------|----------------------|------|-----------|------|
| nA'B'O_3/nA"BO_3 | Q_{RR} | Q_{RR} | Q_{F} | Q_{EF} | Q_{F} | Q_{AF} | P_{001} | P_{110} | P_T | KTaO_3 | - | Pc |
| CdSnO_3 | 0 | 1.22 | 1.85 | 0 | 0 | 0 | 0 | 12.0 | 17.7 | 0 | 0 | 0 | KTaO_3 | - | Pc |
| BaSnO_3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | KTaO_3 | - | Pc |
| 1CdSnO_3/1BaSnO_3 | 1.08 | 0 | 1.21 | 0.20 | 0.60 | 0 | 0 | 9.4 | 12.2 | 8.9 | 13.5 | 16.2 | KTaO_3 | P_4/mmm |
| CdHFO_3 | 0 | 1.27 | 1.74 | 0 | 0 | 0.69 | 0 | 12.3 | 16.9 | 0 | 0 | 0 | KTaO_3 | P_4/mmm |
| BaHFO_3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | KTaO_3 | P_4/mmm |
| 1CdHFO_3/1BaHFO_3 | 1.07 | 0 | 1.17 | 0.18 | 0.64 | 0 | 0 | 9.3 | 12.2 | 7.8 | 10.8 | 13.3 | KTaO_3 | P_4/mmm |
| CaZrO_3 | 0 | 1.02 | 1.82 | 0 | 0 | 0.72 | 0 | 9.2 | 16.2 | 0 | 0 | 0 | MgO | P_4/mmm |
| BaZrO_3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | MgO | P_4/mmm |
| 1CaZrO_3/1BaZrO_3 | 0.79 | 0 | 1.22 | 0.27 | 0.71 | 0 | 0 | 6.6 | 10.8 | 11.1 | 27.6 | 29.7 | MgO | P_4/mmm |
| 1CaZrO_3/1BaZrO_3 | 0.90 | 0 | 1.16 | 0.30 | 0.67 | 0 | 0 | 8.1 | 10.5 | 13.5 | 22.5 | 26.2 | MgO | P_4/mmm |

Strikingly, when A'BO_3 and A"BO_3 form a A'BO_3/A"BO_3 superlattice, the resulting structural distortions are significantly different from their parent bulks. The differences come not only from the amplitudes of the modes but also from the symmetries associated with these modes. In Table III, the OORs around [110] Q_{R_{xy}} are preserved in all these superlattices but, with largely reduced mode amplitudes compared with those in bulk A'BO_3. In contrast, the in-phase OOR around [001] Q_{R} completely disappears and is replaced by a large mode amplitude Q_{R} associated with an out-of-phase OOR around the same axis in all the predicted new materials. As we have seen repeatedly in the previous discussions, such a new pattern of OOR signifies the stabilization of a “BFO-like" structure in all these artificial materials. Accordingly, large polarizations develop along both [001] and [110] directions with the generated total polarization vector roughly along the [111] direction due to the broken symmetry in the e-R3c phase. It can be noted that the polarization of BiFeO_3 is exactly along [111] direction in the R3c symmetry. At the same time, the antipolar mode Q_{AF_{xy}} is completely eliminated. Here, we want to stress that none of the component perovskites in the predicted superlattices is polar either in its natural bulk or in its strained bulk formats!

Outlook

Currently, there are two widely adopted interface approaches to induce FE in oxide superlattices, namely the tricolor [10] and hybrid improper methods [31]. An artificially induced broken inversion symmetry lies at the heart of both the above two methods. In the former, the broken inversion symmetry along the out-of-plane direction is introduced by the number of species in the superlattice; while in the latter, the broken inversion symmetry along the in-plane direction is facilitated by the differences in the antipolar modes of the two perovskite materials across the interface. However, it should be noted that the interface approach discussed here is a new route that is conceptually different from the above. Instead of introducing artificial inversion symmetry breaking, the ferroelectric polarization is stabilized by favoring a “BFO-like" structure which is a metastable phase for many perovskite materials. Due to the nature of the energy term that stabilizes the “BFO-like" structure (∼ R^2_{xy}R_{xy}FE_{xy}FE_{xy}^-), it is expected the switching of FE does not necessarily require switching the directions of oxygen octahedron rotations, which usually requires much larger energy as is implied in the hybrid improper mechanism. Indeed, the FE polarization switching has already been successfully demonstrated in 2BTO/2CTO by Lee’s group [32]. Based on nudged elastic band (transition state) theory [33], [34] and single domain assumption, the energy barrier in switching FE in 2BTO/2CTO (154 meV) is found to be close to that of the predicted materials 1CdSnO_3/1BaSnO_3 (119 meV) both of which are modeled in 40-atom supercells.

In conclusion, by combining HRTEM experimental and first-principles approaches, we introduced a comprehen-
sive interface design method to stabilize a highly polar “BFO-like” metastable phase in perovskite materials. Both the electric and mechanical boundary conditions are taken into account as well. This scheme introduces a conceptually novel way to design artificial FE materials. By predicting some new materials, we demonstrate this approach of exploring novel functional materials. For example, if the FE could be recovered in orthogonal this approach of exploring novel functional materials. For example, if the FE could be recovered in orthogonal RFeO₃(R= Y,Gd, Tb Dy, Ho, Er, Tb, Lu) by this approach, the synthesis of a new family of room temperature multiferroic materials could be achieved. Furthermore, the result of our current work indicates that, through an interface design mechanism, short-period superlattices can have stronger FE than longer ones. This is promising for modern device applications based on ultrathin films.

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