Optimization Model of K-Means Clustering Using Artificial Neural Networks to Handle Class Imbalance Problem

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Abstract. Class imbalance is a situation where instances in one class much higher than instances in other classes. In clustering, this problem not only affects the accuracy of a prediction but also introduces bias in decision-making process. In this case, a machine learning technique will yield a good prediction accuracy from training data class with a large number of instances, but give a poor accuracy in classes with the small number of instances. In this research, we propose an approach for optimizing K-Means clustering in handling class imbalance problem. The approach uses the perceptron feed-forward neural network to determine coordinates of the centroid of a cluster in K-Means clustering processes. Data used in this research are datasets from the UCI Machine Learning Repository. From the experimental results obtained, the proposed approach could optimize the result of K-Means clustering in terms of minimizing class imbalance.

1. Introduction

Class imbalance is a situation where a number of instances in at least one class much higher than the number instances in other classes. This situation creates a majority versus minority class problem. In some particular cases, such as anomaly detection of computer network access patterns, the focus of interest is given more to the minority class since it may contain unusual behaviour differs from the general access patterns [1]. However, in other cases, such as clustering, the focus would be placed on the majority class because it could greatly affect the accuracy of a prediction. A machine learning technique will yield a good prediction accuracy from training data class with a large number of instances, but give a poor accuracy in classes with the small number of instances [2]. In addition, the class imbalance problem also introduces bias in decision-making process as this situation tends to skew rigorously toward the majority class [3].

The focus of this research is to determine the coordinates of the centroid of a cluster in a K-Means clustering process and to analyze its effect to class imbalance. In determining the centroid in the K-Means clustering we proposed the use of perceptron feed-forward neural network. As a supervised learning algorithm, this method is well-known at handling complex pattern recognition. The Various approach had been proposed to minimize the mean square error (MSE) from a simple gradient descent algorithm to more complex distributed autonomous neuro-gen learning engine with distributed adaptive neural network as one of its component [4, 5, 6].

The rest of this paper is organized as follows. In Section 2 we will provide related works concerning the determination of centroid for clustering process as well as the class imbalance problems. In Section...
3 we describe the methodology used in this research and in Section 4 we provide the experimental process performed in this research. Results and discussion are given in Section 5 and finally, we conclude the research in Section 6.

2. Related Works
In the k-means algorithm, deciding the number of clusters and determining the centroid for each cluster are always cumbersome and important tasks since these tasks could directly affect the quality of the resulted clusters. Research works on the determination of the centroid based on fuzzy approach had been done in [7], however, the fuzzy approach has some disadvantages in terms of accuracy for large-size datasets. An approach using new cost function and distance measure based on co-occurrence of values had also been proposed [8]. The intended results are to overcome the limitation of k-means in dealing with numeric data, whereby a modified description of cluster center was presented. Another approach using Fuzzy C-Means (FCM) had been proposed in [9]. The clustering results obtained are integrated into a judgment matrix, which is then iteratively partitioned to identify the desired cluster number and the final result.

Further research using neural networks approach had been proposed in [10] using a modified back-propagation in order to accelerate the learning rate for two-class imbalance problems. This consists of calculating a direction in weight-space which decreases the same amount of errors for each majority and minority classes. Later, [11] corrected errors in the placement of clustering class, despite the correction could overcome the class imbalance. The modified learning algorithm has been proposed for dealing with this problem. A Modified Back Propagation had been proposed in [12] to avoid the ignoring of minority class in a training process in addition to accelerating the convergence of the neural network. More recent work can be found in [13] in which deep neural network training is implemented to handle imbalance datasets. This method equally captured classification errors from both majority class and minority class.

A novel technique with Under Sampled K-Means in handling class imbalance problem had been proposed in [14]. The technique intelligently removed noisy and weak instances from overwhelming (majority) class. However, as formally illustrated in [15], even though the input data for K-Means comes from various true cluster sizes, the resulting clusters are relatively uniform in their sizes. To further dealing with the uniform effect in K-Means, [16] used the Visual K-Means algorithm for skewed distributed data sources. They argued that the proposed algorithm could effectively handle the imbalanced datasets.

3. Methods
The data used in this research are the Balanced Scale and Abalone Datasets from the UCI Machine Learning Repository. In general, the methodology consists of two stages: preparation stage and the clustering stage. In the preparation stage, the dataset is trained by a perceptron neural network to generate \( k \) initial cluster centers (centroids) in which for the Balanced Scale dataset there are three classes, namely Class B, Class L, and Class R while in the Abalone dataset the clusters are Sex F, Sex I, and Sex M. In this research, the generated \( k \) centroids are used as the initial cluster centers for the k-means clustering. The general architecture of the proposed method used is depicted in Fig. 1.

![Figure 1. The general architecture](image-url)
The modification of K-means clustering algorithm in determining centroid using perceptron are shown as follows.

**Input:** The Number of Cluster $k$ and a database containing $n$ objects

**Output:** A set of $k$ clusters which minimize the squared-error criterion

**Method:**

1. Calculate the initial cluster centers of $k$ objects using perceptron.
2. Repeat until convergence
   1. (Re) assign each object to the cluster to which the object is the most similar, based on the mean value of the objects in the cluster.
   2. Update the cluster means, i.e., calculate the mean value of the objects for each cluster.
3. }

As for the original K-Means Algorithm and the modified K-Means Algorithm using Perceptron are shown in Fig. 2 and 3.

**Figure 2.** The original K-Means algorithm

**Figure 3.** The modified K-Means algorithm using Perceptron

The algorithm of calculating the initial cluster centers (centroid) of $k$ objects using perceptron are shown as follows.

1. Initialize weight and bias
   - Set learning rate
   - Set input according to dataset

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Set target according to cluster of data from dataset

Step 2. While stopping condition is false, do steps 3-6

Step 3. For each training pair s,t, do steps 4-5

Step 4. Set activations of input units:
\[ x_i = s_i \]

Step 5. Compute response of output unit:
\[ y_{in} = b + \sum_i x_i w_i \]
\[ y = \begin{cases} 
1, & \text{if } y_{in} > 0 \\
0, & \text{if } -0 \leq y_{in} \leq 0 \\
-1, & \text{if } y_{in} < -0 
\end{cases} \]

Step 6. Update weights and bias if an error occurred for this pattern.
If \( y \neq t \)
\[ w_i(\text{new}) = w_i(\text{old}) + \alpha t x_i \]
\[ b(\text{new}) = b(\text{old}) + \alpha t \]
else
\[ w_i(\text{new}) = w_i(\text{old}) \]
\[ b(\text{new}) = b(\text{old}) \]

Step 7. Test stopping condition
if no weights changed in Step 3, stop; else, continue Step 2.

4. Experimental Process
4.1. Dataset Description
The dataset used in this experiment are the Balanced Scale and Abalone datasets from the UCI Machine Learning Repository.

4.2. Determining the Number of Clusters
The number of clusters K in this study is 3 in accordance with the classes in the Balanced Scale dataset and the Abalone dataset. There are 4 (four) attributes in Balanced Scale dataset: Left-Weight, Left-Distance, Right-Weight, and Right-Distance and the Abalone dataset has 8 (eight) attributes: Length, Diameter, Height, Whole Weight, Shucked Weight, Viscera Weight, Shell Weight, and Rings.

4.3. Determining the Centroid of K-Means
Determining the centroid of K-Means using Artificial Neural Network can be divided into three steps: determining the centroid for each cluster, and each step has a step as follows (in this section, the example is given for Cluster Class B in Balanced Scale Dataset)

Step 1. Initialize weight and bias
Set learning rate
Set input according to dataset
Set target according to cluster of data from dataset

Step 2. Step 1-6. Training process for determining the centroid for Class B

The Training process of determining the centroid for Class B can be seen in Table 1.
Table 1. Training process in determining the centroid of Class B (Epoch 1)

| Input | Weight | Final Weight |
|-------|--------|--------------|
| X1    | X2     | X3 | X4 | Target | W1 | W2 | W3 | W4 | Actual | Error | W1 | W2 | W3 | W4 |
| 1     | 1      | 1  | 1  | 0      | 0  | 0  | 0  | 0  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 1     | 2      | 1  | 2  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 1     | 3      | 1  | 3  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 1     | 4      | 1  | 4  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 2     | 3      | 2  | 3  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 3     | 4      | 3  | 3  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 4     | 1      | 4  | 1  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 3     | 5      | 5  | 3  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 5     | 2      | 2  | 5  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |
| 5     | 5      | 5  | 5  | 0.1   | 0.1 | 0.1 | 0.1 | 1  | 0      | 1    | 0.1 | 0.1 | 0.1 | 0.1 |

The maximum number of epochs in this study is 200. The training process were done using the R Language. Fig. 4, Fig. 5, and Fig. 6 are the training process in determining the centroid of the Class B, Class L, and Class R. Fig. 7 is the result of Centroid from training process.

Figure 4. Training Process in Determining Class B

Figure 5. Training Process in Determining Class L
From the Fig. 4, 5, and 6 can be seen that the training process get the minimum error in epoch 10, actually, the maximum number of epochs is 200. The Fig. 7 show us the Centroid of Left-Weight, Left-Distance, Right-Weight, and Right-Distance in determining Class B, Class L, and Class R.

The training process were done using the R Language. Fig. 8, Fig. 9, and Fig. 10 are the training process in determining the centroid of the Abalone Class Sex F, Abalone Class Sex I, and Abalone Class Sex M. Fig. 11 is the result of Centroid from training process.
5. Results and discussion

Results of the original K-Means clustering for Balanced Scale and Abalone datasets, can be seen in Table 2.

| Testing Number | Number of Error | Number of Data in Class 1 | Number of Data in Class 2 | Number of Data in Class 3 |
|----------------|-----------------|---------------------------|---------------------------|---------------------------|
|                | Balanced Scale  | Abalone                   | Balanced Scale            | Abalone                   | Balanced Scale            | Abalone                   |
| 1              | 383             | 2430                      | 276                       | 910                       | 196                       | 3073                      | 153                       | 194                       |
| 2              | 435             | 2499                      | 200                       | 824                       | 149                       | 3217                      | 276                       | 136                       |
| 3              | 480             | 3262                      | 281                       | 2722                      | 145                       | 1194                      | 199                       | 261                       |
| 4              | 493             | 2488                      | 152                       | 2281                      | 201                       | 449                       | 272                       | 1447                      |
| 5              | 481             | 2486                      | 266                       | 194                       | 194                       | 3212                      | 165                       | 771                       |
| 6              | 383             | 2937                      | 155                       | 2722                      | 196                       | 261                       | 274                       | 1194                      |
| 8              | 401             | 3262                      | 211                       | 2722                      | 135                       | 1194                      | 297                       | 261                       |
| 9              | 396             | 3331                      | 165                       | 2095                      | 256                       | 1592                      | 204                       | 490                       |
| 10             | 403             | 2771                      | 244                       | 1194                      | 225                       | 261                       | 156                       | 2722                      |

Average 385.5 2546.6

From Table 2, it can be seen that in both Balanced Scale and Abalone datasets clustering there are class imbalance problem. The number of Data in Class 1, Class 2, and Class 3 in Balanced Scale and Abalone datasets can be very different in Size. As the result of this class imbalance, we can see that the number of error that occur is quite large. The average of error in Balanced Scale is 385.5 (61.68%) and the average of error in Abalone is 2546.6 (60.96%)

Results of the clustering using the optimization model of K-Means in determining the centroid of both Balanced Scale and Abalone datasets we can see the in Table 3.
Table 3. Results of Balanced Scale and Abalone datasets with the optimization model of K-Means clustering

| Dataset       | Number of Error | Number of Data in Class 1 | Number of Data in Class 2 | Number of Data in Class 3 |
|---------------|-----------------|----------------------------|----------------------------|---------------------------|
| Balanced Scale| 289             | 202                        | 186                        | 237                       |
| Abalone       | 2166            | 1182                       | 2035                       | 960                       |

From the Table 3, it can be seen that the optimization model of K-Means Clustering can reduce the number of Errors. For Balanced Scale dataset the number of errors were decreased to 289 or about 46.24%, whereas clustering result of Abalone dataset has reduced the number of errors to 2166 or about 51.86%.

By comparing the results of Table 2 and Table 3, it can be seen that the number of errors of both Balanced Scale and Abalone datasets has been reduced using the optimization model of K-Means clustering and it has a better performance than the result of [17]. It gave the number of error of 50% using K-Modes in Balanced Scale dataset and in Abalone dataset has the slightly below performance with another result from [18], that the result of [18] gave the number of error of 38.22 using modified K-Means but still has a better performance than the result of [18] that using Hierarchical Clustering that gave the number of error of 93.77%.

6. Conclusion
The conclusion of this research are as follows. First, the Artificial Neural Network can determine the centroid of K-Means Clustering, it was indicated by decreasing the number of errors. Second, it is confirmed that the Optimization Model of K-Means Clustering using Artificial Neural Network also can handle the class imbalance problem.

Our case study is using numerical datasets and in the future, it should be another study on non-numerical datasets and the average number of error can be reduced using more iteration. The importance of this research for future studies is that the results indicate that proper determination of the centroid can reduce the occurrence of class imbalance.

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