The Effects of La Doping on the Crystal Structure and Magnetic Properties of Ni$_2$In-Type MnCoGe$_1$–$_x$La$_x$ (x = 0, 0.01, 0.03) Alloys

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Abstract: In this experiment, a series of MnCoGe$_1$–$_x$La$_x$ (x = 0, 0.01, 0.03) alloy samples were prepared using a vacuum arc melting method. The crystal structure and magnetic properties of alloys were investigated using X-ray diffraction (XRD), Rietveld method, physical property measurement system (PPMS), and vibrating sample magnetometer (VSM) analyses. The results show that all samples were of high-temperature Ni$_2$In-type phases, belonging to space group P6$_3$/mmc (194) after 1373 K annealing. The results of Rietveld refinement revealed that the lattice constant and the volume of MnCoGe$_1$–$_x$La$_x$ increased along with the values of La constants. The magnetic measurement results show that the Curie temperatures (T$_C$) of the MnCoGe$_1$–$_x$La$_x$ series alloys were 294, 281, and 278 K, respectively. The maximum magnetic entropy changes at 1.5T were 1.64, 1.53, and 1.56 J·kg$^{-1}$·K$^{-1}$, respectively. The respective refrigeration capacities (RC) were 60.68, 59.28, and 57.72 J·kg$^{-1}$, with a slight decrease along the series. The experimental results show that the doping of La results in decreased T$_C$, basically unchanged magnetic entropy, and slightly decreased RC.

Keywords: MnCoGe alloy; rare earth doping; Rietveld full spectrum fitting; crystal structure; magnetic properties

1. Introduction

Heusler alloy is an intermetallic compound characterized by a highly ordered arrangement of atoms. It can be divided into full Heusler alloy and half-Heusler alloy, which provides the material with rich physical properties and application functions [1]. Heusler alloy has not only the properties of a metal alloy but also significant magnetic properties [2–5]. MM’X alloy is a kind of Heusler alloy, of which the MM’X alloy MnCoGe has attracted wide attention [6–14]. MnCoGe has an orthogonal TiNiSi-type (space group Pnma(64)) structure at room temperature. As the temperature increases, the alloy undergoes a magnetic phase transition at ~345 K [15]. Specifically, at 650 K, the first order structure phase transitions from an orthogonal TiNiSi phase to a high-temperature hexagonal Ni$_2$In-type (space group P6$_3$/mmc (194)) [15], and the Curie temperature is T$_C^{1H}$ ~275 K [16]. During the alloy cooling process, there is a phase transformation from hexagonal to orthorhombic that occurs, which is a non-diffusion type of lattice distortion referred to as a martensitic transformation. It can be seen that the magnetic phase transition and structural phase transition in MnCoGe alloy are separate processes. In order to increase the amount of change in magnetization during the phase transition process needed to obtain a large magnetocaloric effect, it is necessary to adjust the structural phase transition temperature to a point between the two-phase Curie temperature window to couple the structural phase transition with the magnetic transition.

In recent years, many studies have been conducted on the phase transition control of the magnetic structure of MnCoGe-based alloys. It has been shown that the martensitic
phase transition temperature of MnCoGe-based alloys is more sensitive to pressure and chemical composition. The doping of trace elements or the application of pressure can be effective in significantly regulating the martensite transformation temperature. At present, there are four main methods for regulating the phase transition temperature of MnCoGe-based alloy Martensite: interstitial atom doping [13], transition element and/or main group element absence (excess) [5,17], transition element and/or main group element substitution [7], and external application pressure [8,18,19].

In 2017, Hassan et al. reduced the phase transition temperature of MnCoGe$_{1+x}$ alloy by adding excessive main group element Ge and realized a magnetic and structure coupled phase transition [17]. Trung et al. first reported the giant magnetocaloric effect of MnCoGe alloy in 2010. The alloy is doped with B atoms and with the increase in B element doping, the martensite transformation temperature is reduced and the giant magnetocaloric effect is realized under a certain composition [20]. Liu et al. calculated the total energies of Mn vacancies and co-vacancies in the Ni$_2$In structure by first principles (ab initio method), and the results confirmed that the co-vacancy structure (Mn$_{1-x}$Co$_x$)(Co$_{1-x}$Ge is energetically favorable. Therefore, by introducing Mn vacancies into the system, the coupling of magnetic and structural phase change was successfully realized by using the favorable Co vacancy, and a phase change window of about 100 K was found [21]. In 2016, Bao Lifu et al. realized magnetic and structure coupled phase transition and the resulting giant magnetocaloric effect in the MnCoGe$_{1-x}$ alloy through the absence of the non-magnetic atom Ge [9]. In 2014, Shen et al. found that the substitution of Zn for Mn led to the coupling of phase transitions in the magnetic structure, and a large room temperature magnetocaloric effect was obtained. The magnetic entropy of the Mn$_{0.96}$Zn$_{0.04}$CoGe alloy reached a peak value of 4.3 J·kg$^{-1}$K$^{-1}$ when the magnetic field was changed from 0 to 0.1 T [6].

At the same time, rare earth permanent magnet materials also have excellent properties and are widely used in many fields. However, rare earth permanent magnets use a large amount of only Pr, Nd, Tb, and Dy, which leads to the unbalanced utilization of rare earth resources. Pr, Nd, Tb, and Dy resources are scarce, while La and Ce resources are abundant and overstocked. Therefore, in recent years, the development of magnetic materials containing La and Ce has become the focus of attention in academia and industrial production [22–25].

As an important half-Heusler alloy, MnCoGe has been studied in significant detail. The MnCoGe Heusler alloy can be applied to refrigeration equipment and zero-expansion materials due to its unique magnetic refrigeration, magnetocaloric and negative thermal expansion effects. It has huge development potential [26–28]. However, most of the samples currently studied are not single-phase, and most of the research samples are two-phase. There are few studies on the doping of high-temperature Ni$_2$In-phase MnCoGe single-phase samples, and the doping of rare earth La atoms in high-temperature Ni$_2$In-phase MnCoGe alloy has not previously been studied. As such, the study of the magnetic properties of La-doped high-temperature Ni$_2$In phase MnCoGe alloy is meaningful for its potential application.

2. Experimental Method

In this experiment, MnCoGe$_{1-x}$La$_x$ ($x = 0, 0.01, 0.03$) were prepared using a high-temperature melting method. The purities of the raw materials Mn, Co, Ge, and La were 99.9%, 99.99%, 99.9999%, and 99.95%, respectively. Under the protection of pure argon (argon purity is 99.9999%) and using a vacuum electric arc furnace for smelting, the raw materials were smelted four times in order to ensure that the composition of the alloy ingots were uniform. Then, the ingots were placed in a quartz tube under vacuum at 1373 K for 72 h, followed by quenching with a mixture of ice and water.

A Rigaku D/max-2500 X-ray diffractometer with CuKα radiation source was used to analyze sample purity. The Rietveld method in FullProf program was used to refine the crystal structure of the sample. The magnetic properties of the samples were measured...
using a comprehensive physical property measurement system (PPMS; Quantum Design, USA), in which the temperature range and maximum magnetic field intensity were 5–400 K and ±5 T; and a vibrating sample magnetometer (model Lake Shore 7410), in which the temperature range and maximum magnetic field intensity were 100–420 K, and ±1.6 T.

3. Results and Discussion

Figure 1 shows the powder XRD patterns of the MnCoGe$_{1-x}$La$_x$ (x = 0, 0.01, 0.03) samples measured at room temperature. The XRD data of the MnCoGe$_{1-x}$La$_x$ series alloy samples were analyzed using Jade5.0 software. The results show that the samples were single phase after annealing. The structure of the single phase is a high-temperature Ni$_2$In-type MnCoGe phase and the space group is P6$_3$/mmc (194). These results are in good agreement with those reported by the Central Research Department [27]. The inset in Figure 1 is a partial enlarged view of sample XRD at 42–45.5°. As the figure shows, the positions of the strongest peak and the second strongest peak shift to a low angle with the increase in doped content, which reflects the increase in lattice that occurs with the increase in doped content.

Figure 1. XRD pattern of MnCoGe$_{1-x}$La$_x$ alloy at room temperature.

In order to further determine the composition of the sample, MnCoGe$_{1-x}$La$_x$ (x = 0, 0.01, 0.03) series of alloys were analyzed by SEM/EDS. Figure 2 presents the EDS patterns of MnCoGe$_{1-x}$La$_x$ alloys. According to the analysis results on the EDS data obtained from scanning electron microscope, seen in Figure 2, this series of alloys are single phase, which agreed well with the results of XRD. It can be seen that the sample in Figure 2a with the composition Mn33.60Co32.42Ge33.98 was determined to be MnCoGe and that in Figure 2b with the composition Mn33.57Co33.55Ge32.84La0.04 was assigned to be MnCoGe$_{1-x}$La$_x$ (x = 0.01). The composition of the sample in Figure 2c is Mn33.96Co33.26Ge32.73La0.08, indicating the sample contained the single phase of MnCoGe$_{1-x}$La$_x$ (x = 0.03). These results are all in good agreement with those of XRD analysis.
The crystal structure parameters of the high-temperature Ni$_2$In-type MnCoGe (space group P6$_3$/mmc (194)), in which the La atoms replace part of the Ge atom positions, were used as the initial data, and were input into the computer program FullProf. The peak shape function of the fitting correction is the pseudo-Voigt function. A total of 25 parameters were refined during Rietveld refinement, including lattice parameters, half-width, preferred orientation factor, symmetry, and isotropic temperature factor. Finally, the Rietveld refinement results of the MnCoGe$_{1-x}$La$_x$ series alloy samples were obtained.

Figure 3 shows the Rietveld refinement pattern of the MnCoGe$_{1-x}$La$_x$ series alloy samples. From this pattern, the experimental values, calculated values, and residuals can be observed. The reliability of the Rietveld refinement results is reflected by the residual variance factor $R_P$ of the graph and the residual variance factor $R_{WP}$ of the weighted graph. The expression is:

$$R_P = \frac{\sum Y_i(\text{obs}) - Y_i(\text{calc})}{\sum Y_i(\text{obs})} \quad (1)$$

$$R_{WP} = \left\{ \frac{\sum wi[Y_i(\text{obs})^2 - Y_i(\text{calc})^2]}{\sum wi[Y_i(\text{obs})^2]} \right\}^{1/2} \quad (2)$$

The Rietveld refinement effect can be judged by the size of the residual. The smaller the $R_P$ and $R_{WP}$ values, the more reliable the results. The Rietveld refinement results of the MnCoGe$_{1-x}$La$_x$($x = 0, 0.01, 0.03$) samples are shown in Table 1. From the values of $R_P$, $R_{WP}$, and $R_{EXP}$ in Table 1, it can be observed that the Rietveld refinement results are credible. As the doped amount increases, the lattice constants $a$, $b$, and $c$ of the high-temperature Ni$_2$In-type MnCoGe gradually increase. The unit cell volume also gradually increases. This is because the La atomic radius (1.87 Å) is larger than the Ge atomic radius (1.40 Å), which causes the crystal lattice to become larger. Table 2 shows the results of the site occupation and the occupancy of various atoms in refined MnCoGe$_{1-x}$La$_x$.
Figure 3. Rietveld refinement results for MnCoGe$_{1-x}$La$_x$: (a) MnCoGe; (b) MnCoGe$_{0.99}$La$_{0.01}$; (c) MnCoGe$_{0.97}$La$_{0.03}$.

### Table 1. Rietveld refinement result for MnCoGe$_{1-x}$La$_x$ series alloy.

| Compounds            | MnCoGe          | MnCoGe$_{0.99}$La$_{0.01}$ | MnCoGe$_{0.97}$La$_{0.03}$ |
|----------------------|-----------------|-----------------------------|-----------------------------|
|                      | Space group     | Radiation                   |                             |
|                      | P6$_3$/mmc (194) | CuK$\alpha$                 |                             |
| Unit cell parameters |                 |                             |                             |
| a/(Å)                | 4.0641(1)       | 4.0648(1)                   | 4.0695(1)                   |
| b/(Å)                | 4.0641(1)       | 4.0648(1)                   | 4.0695(1)                   |
| c/(Å)                | 5.2882(2)       | 5.2905(2)                   | 5.2980(2)                   |
| Lattice volume V(Å³) | 87.337(5)       | 87.430(7)                   | 87.761(2)                   |
| Reliability factors  |                 |                             |                             |
| $R_p$ (%)            | 12.9            | 13.3                        | 13.0                        |
| $R_{WP}$ (%)         | 15.5            | 15.7                        | 15.7                        |
| $R_{exp}$ (%)        | 5.14            | 4.96                        | 4.96                        |
Table 2. Atomic site occupation and occupancy rate of MnCoGe$_{1-x}$La$_x$.

| Doping Content $x$ | Atoms   | Site Occupation | $x$ | $y$ | $z$ | Occupancy |
|---------------------|---------|----------------|-----|-----|-----|-----------|
| 0                   | Mn      | 2a             | 0   | 0   | 0   | 1         |
|                     | Co      | 2d             | 1/3 | 2/3 | 3/4 | 1         |
|                     | Ge      | 2c             | 1/3 | 2/3 | 1/4 | 1         |
| 0.01                | Mn      | 2a             | 0   | 0   | 0   | 1         |
|                     | Co      | 2d             | 1/3 | 2/3 | 3/4 | 1         |
|                     | Ge      | 2c             | 1/3 | 2/3 | 1/4 | 0.993Ge + 0.007La |
| 0.03                | Mn      | 2a             | 0   | 0   | 0   | 1         |
|                     | Co      | 2d             | 1/3 | 2/3 | 3/4 | 1         |
|                     | $M_1$*  | 2c             | 1/3 | 2/3 | 1/4 | 0.976Ge + 0.024La |
|                     | $M_2$** | 2c             | 1/3 | 2/3 | 1/4 | 0.976Ge + 0.024La |

* $M_1 = 0.993$Ge + 0.007La; ** $M_2 = 0.976$Ge + 0.024La.

Figure 4a shows the crystal structure of the MnCoGe$_{0.97}$La$_{0.03}$ alloy. The pink and purple spheres in the figure are Mn and Co atoms, and the dark green and green spheres are $M_2$ atoms. The green part is Ge atoms, and the dark green part is doped La atoms. Figure 4b–d are the atomic environments of Mn, Co, and $M_2$ atoms. As can be observed, the Mn atom is linked with two adjacent Mn atoms, six adjacent Co atoms, and six adjacent $M_2$ atoms. Six adjacent Mn atoms and five adjacent $M_2$ atoms are connected with the central Co atom. The Mn atom is connected to six adjacent Mn atoms and five adjacent Co atoms. From Table 3, it can also be observed that the bond length changes after refinement. It can also be argued that the Mn–Mn and Mn–Co distances become longer due to increasing doped La content.

In this study, the magnetic properties of MnCoGe$_{1-x}$La$_x$ ($x = 0, 0.01, 0.03$) series alloy samples were measured using a comprehensive physical property measurement system (PPMS; Quantum Design, USA) and vibrating sample magnetometer (model Lake Shore 7410).

Figure 4. MnCoGe$_{0.97}$La$_{0.03}$ crystal structure: (a) the crystal structure of the MnCoGe$_{0.97}$La$_{0.03}$; (b) the atomic environments of Mn; (c) Co and (d) $M_2$. 
Table 3. The number of different atoms of each central atom and its nearest neighbor.

| Central Atom | Connected to the Atom | Atomic Number | Distance (Å) |
|--------------|-----------------------|---------------|--------------|
|              |                       |               | 0  | 0.01 | 0.03 |
| Mn           | Mn                    | 2             | 2.6441(10)   | 2.6453(10) | 2.6490(10) |
| Co           | Co                    | 6             | 2.6930(7)    | 2.6937(8)  | 2.6970(8)  |
| Ge/M₁/M₂     | Ge/M₁/M₂              | 6             | 2.6930(7)    | 2.6937(8)  | 2.6970(8)  |
| Mn           | Mn                    | 6             | 2.6930(7)    | 2.6937(8)  | 2.6970(8)  |
| Co           | Ge/M₁/M₂              | 5             | 2.3462(6)    | 2.3466(8)  | 2.3493(8)  |
| Ge/M₁/M₂     | Mn                    | 6             | 2.6930(7)    | 2.6937(8)  | 2.6970(8)  |
| Co           | Co                    | 5             | 2.3462(6)    | 2.3466(8)  | 2.3493(8)  |

Figure 5 shows the temperature dependence of the magnetization (M) of MnCoGe₁₋ₓLaₓ series alloy samples in an external magnetic field of 0.05 T (MT curves). Here, T_C is defined as the temperature at which the maximum slope occurs during zone field cooling (FC), where T_C represents the general meaning of the T_C that is the transition temperature between the FM and PM phases. The inset in the figure shows the spectrum of the dM/dT curve. The peak position on the right is Tc. When x = 0, 0.01, and 0.03, the corresponding Tc values of MnCoGe₁₋ₓLaₓ alloys are 294, 281, and 278 K, respectively. With an increase in doped La content, the Curie temperature shows an obvious downward trend. An obvious thermal hysteresis in the field cooling (FC) and field cooling heating (FCH) curves near the Curie temperature can be clearly observed. This thermal hysteresis is caused by the martensitic transformation in the MnCoGe₁₋ₓLaₓ series alloys, which confirms the first-order nature of the transformation. Thermal hysteresis also shows that the magnetic structure transition is not coupled.

Figure 5. Cont.
Figure 5. Temperature dependence of magnetization of (a) MnCoGe, (b) MnCoGe$_{0.99}$La$_{0.01}$, and (c) MnCoGe$_{0.97}$La$_{0.03}$ measured under a magnetic field of 500 Oe.

The curve of $\chi^{-1} \sim T$ is shown in Figure 6. It can be found that the reciprocal of the magnetic susceptibility of MnCoGe$_{1-x}$La$_x$ ($x = 0$, 0.01, 0.03) alloys in the high-temperature
region varies linearly with temperature, indicating that these compounds obey the Curie–Weiss law:

$$\chi = \frac{C}{T - \theta_C}.$$  

(3)

The green lines in Figure 6 are the curve of the reciprocal of the magnetic susceptibility with temperature, and the blue lines are the Curie–Weiss fitting. The Curie constant $C$ and the Curie–Weiss temperature $\theta_C$ can be calculated separately by fitting the curve linearly.

From the fitting curve analysis of Figure 6, the Curie constants of $\text{MnCoGe}_{1-x}\text{La}_x$ can be obtained as 0.0181 (2), 0.0179 (2), and 0.0174(3), respectively. Moreover, the Curie–Weiss temperatures $\theta_C$ of $\text{MnCoGe}_{1-x}\text{La}_x$ are 300.36, 291.36, and 289.97 K, respectively. The expression of the Curie constant $C$ is as follows:

$$C = \frac{N_A\mu_B^2}{3K_B}\mu_{\text{eff}}^2.$$  

(4)

Among the various constants in the expression are the Avogadro constant, $N_A = 6.023 \times 10^{23} \text{ mol}^{-1}$; the Bohr constant, $\mu_B = 9.274 \times 10^{-21} \text{ emu}$; and the Boltzmann constant, $k_B = 1.380649 \times 10^{-23} (\text{J} \cdot \text{K}^{-1})$. The reciprocal of the magnetic susceptibility $\chi^{-1}$ and the reciprocal of the slope of the linear part of the temperature (T) curve in the high-temperature region are the Curie constant $C$. The above formula can be simplified to:

$$\mu_{\text{eff}}(\mu_B) = \sqrt{8.0028 \times C \times M}.$$  

(5)

where $M$ is the relative molecular mass. By substituting the fitted values into the formula, it can be calculated that the effective magnetic moments of $\text{MnCoGe}_{1-x}\text{La}_x$ are 5.20, 5.17, and 5.12 $\mu_B$, respectively. It can also be observed that, with the doping of La, the effective magnetic moment gradually decreases. Due to La doping, the Mn–Mn distance in the compound becomes larger, which weakens the interaction between Mn atoms. Wang et al. [16,29] demonstrated that the smaller Mn–Mn distance separation in hexagonal Ni2In-type MnCoGe-based alloys results in a wider 3d band width and less exchange split between the majority band and minority bands. Therefore, the moment of the system is generally smaller. Moreover, it has been proven that by changing the intercrystalline bond length of the material, the generated three-dimensional band can reduce electron splitting exchange interaction, thereby reducing the net magnetic moment.

Table 4 shows the values of various parameters obtained after the Curie–Weiss fitting of $\text{MnCoGe}_{1-x}\text{La}_x$. From the comparison between the Curie–Weiss temperature and the Curie temperature in the table, it is clear that the two temperature values are close. It can also be seen that the fitting results are reasonable.

| Doping Content $x$ | $T_C$/K | $\theta_C$/K | $C$ | Effective Magnetic Moment($\mu_B$/Formula) |
|---------------------|---------|-------------|-----|------------------------------------------|
| 0                   | 294     | 300.36(2)   | 0.0181(2) | 5.20                                    |
| 0.01                | 281     | 291.36(5)   | 0.0179(2) | 5.17                                    |
| 0.03                | 278     | 289.97(3)   | 0.0174(3) | 5.12                                    |

It can be seen from Figure 7a that the $\text{MnCoGe}_{1-x}\text{La}_x$ ($x = 0.01$) alloy is in a paramagnetic state at 300 K and in a ferromagnetic state at 80 K. From Figure 7b, the sample $\text{MnCoGe}_{1-x}\text{La}_x$ ($x = 0.03$) is not completely converted to paramagnetism at 300 K, but still has ferromagnetic behavior. According to Bohol’s law [30], one can draw the $M$–$H^{-1}$ curve and extrapolate the linear part to $H^{-1} = 0$ to obtain the saturation magnetization of $M_S$. As can be seen from Figure 7a, the saturation magnetizations of $\text{MnCoGe}$ and $\text{MnCoGe}_{0.97}\text{La}_{0.03}$ at 80 K are 88.75 and 87.55 emu/g, respectively, and there is no coercivity. In Figure 7b, it is apparent that the saturation magnetization of $\text{MnCoGe}_{0.97}\text{La}_{0.03}$ at 5 K is
80.91 emu/g. No coercivity was observed in this series of compounds, indicating that the compounds can be used as soft magnetic materials.

Figure 6. $\chi^{-1}$–T fitting curves of MnCoGe$_{1-x}$La$_x$: (a) MnCoGe; (b) MnCoGe$_{0.99}$La$_{0.01}$; (c) MnCoGe$_{0.97}$La$_{0.03}$.

Figure 7. M–H curves of MnCoGe$_{1-x}$La$_x$ measured at different temperatures: (a) MnCoGe and MnCoGe$_{0.99}$La$_{0.01}$; (b) MnCoGe$_{0.97}$La$_{0.03}$.

The isothermal magnetization curve (MH) of MnCoGe$_{1-x}$La$_x$ series alloys was measured, and the temperature ranges are 228–320, 218–320, and 228–330 K. The temperature interval is 2 K, as shown in Figure 8a,c,e. Figure 8b,d,f shows the corresponding Arrott curve ($M^2$–H/M) and the Arrott curve made from the isothermal magnetization (M–H).
curve, which can be used as the basis for evaluating the magnetic phase change. Experimentally, the type of magnetic phase transition can be determined by the slope in the Arrott curve. Generally speaking, a positive slope corresponds to a second-order phase transition, and a negative slope corresponds to a first-order phase transition. In this work, all Arrott curves show a positive slope near the Curie temperature, revealing the characteristics of the second-order phase transition (SOMT) based on the Banerjee criterion [30]. Magnetic refrigeration materials require a secondary phase change from FM (ferromagnetic) to PM (paramagnetic) because the primary phase change is accompanied by hysteresis loss. It is apparent in the results that MnCoGe$_{1-x}$La$_x$ series alloys meet this characteristic.

Figure 8. Isothermal magnetization curves (a,c,e) and Arrott curves (b,d,f) of MnCoGe$_{1-x}$La$_x$ at different temperatures.
According to the related theories of thermodynamics, the magnetocaloric effect of materials can be calculated by using the Maxwell relationship:

$$\left(\frac{\partial M}{\partial T}\right)_H = \left(\frac{\partial S}{\partial H}\right)_T$$

(6)

Isothermal magnetic entropy change is obtained by the isothermal magnetization curve, which can be described by the following formula:

$$\Delta S_M(T, H_{\text{max}}) = S_M(T, H_{\text{max}}) - S_M(T, 0) = \int_0^{H_{\text{max}}} \left(\frac{\partial M}{\partial T}\right)_H dH$$

(7)

Here, $S$, $M$, $H$, and $T$ represent entropy, magnetization, magnetic field, and temperature, respectively. A series of isothermal magnetic entropy changes around the phase transition temperature of the sample can be approximated as:

$$\Delta S_M(T, H) = \sum_i \frac{M_{i+1}(T_{i+1}, H) - M_i(T_i, H)}{T_{i+1} - T_i} \Delta H$$

(8)

Using Maxwell’s relationship, the isothermal magnetic entropy change in the second-order phase change material is calculated from the isothermal magnetization curve. Figure 9 shows the results of isothermal magnetic entropy changes in MnCoGe$_{1-x}$La$_x$ alloy magnetization. The magnetic entropy changes in MnCoGe, MnCoGe$_{0.99}$La$_{0.01}$, and MnCoGe$_{0.97}$La$_{0.03}$ change the most near the magnetic transition temperature, while they increase with the increase in the external magnetic field. Under an external magnetic field of 1.5T, the maximum magnetic entropy changes $|\Delta S_M|$ of MnCoGe, MnCoGe$_{0.99}$La$_{0.01}$, and MnCoGe$_{0.97}$La$_{0.03}$ are 1.64, 1.53, and 1.56 J·kg$^{-1}$·K$^{-1}$.

It can be seen that the magnetic entropy changes in the alloy samples have no obvious changes in relation to the doping of La atoms, as they were decreased compared to MnCoGe$_{0.99}$Ga$_{0.05}$ [31] and MnCoGe$_{0.98}$Al$_{0.02}$ [32], among others. However, the specific mechanism is not clear. The reduction in transition temperature and magnetic entropy change may be the result of a combination of many factors. The change in the covalent bond and local environment could be the cause of the decrease in $|\Delta S_M|$ [33]. In addition, doping the Ge site with a less electronegative La element will result in a stronger Mn–Mn bond (Pauling—electronegativity of Ge and La are 2.01 and 1.158, respectively) [34], thereby reducing the transition temperature and magnetic entropy change, which is similar in the cases of MnCo$_{1-x}$Cd$_x$Ge [33], MnCoGe$_{1-x}$Si$_x$ [34], and MnCoGe$_{1-x}$Al$_x$ [32].

Although the basic requirement for magnetic refrigeration materials is a large magnetic entropy change, a material with a large magnetic entropy change $|\Delta S_M|$ cannot guarantee high refrigeration efficiency. The recognized standard for evaluating refrigeration efficiency is refrigeration capacity (RC), which represents the amount of heat transfer in a thermodynamic cycle. The value of refrigeration capacity (RC) is measured by different methods. In this article, RC value is calculated using the method proposed by Gschneidner et al. based on the following formula:

$$\text{RC} = \frac{T_{\text{hot}}}{T_{\text{cold}}} \int_{T_{\text{cold}}}^{T_{\text{hot}}} \Delta S(T) dT$$

(9)

In the formula, $T_{\text{hot}}$ and $T_{\text{cold}}$ correspond to the temperature range of $|\Delta S_M|$, which is half of the highest peak value. The value of the temperature span of the entire width, corresponding to a half-maximum (FWHM) value of $|\Delta S_M|$, is the difference between $T_{\text{hot}}$ and $T_{\text{cold}}$ (expressed as $\delta T_{\text{FWHM}}$, where $\delta T_{\text{FWHM}} = T_{\text{hot}} - T_{\text{cold}}$). Under a magnetic field of 1.5 T, the $\delta T_{\text{FWHM}}$ values of the $|\Delta S_M|$ for the MnCoGe$_{1-x}$La$_x$ alloys are 37, 39, and 37 K for $x = 0$, 0.01, and 0.03, respectively. For $\Delta H = 1.5$ T, the refrigeration capacity (RC$_{\text{FWHM}}$) values for the MnCoGe$_{1-x}$La$_x$ alloys are 60.68, 59.28, and 57.72 J·kg$^{-1}$ for $x = 0$, 0.01, and 0.03, respectively.
0.01, and 0.03, respectively. For $\Delta H = 1$ T, the refrigeration capacity ($RC_{\text{FWHM}}$) values for the MnCoGe$_{1-x}$La$_x$ alloys are 38.44, 36.16, and 34.8 J kg$^{-1}$ for $x = 0$, 0.01, and 0.03, respectively. Table 5 shows MCE of MnCoGe$_{1-x}$La$_x$ alloys compared with other materials.

Table 5. The MCE of MnCoGe$_{1-x}$La$_x$ alloys compared with other materials.

| Materials                  | Magnetic Field/T | $|\Delta S_M|/J \cdot kg^{-1} \cdot K^{-1}$ | $T_{pk}/K$ | $RC/J \cdot kg^{-1}$ | $\delta T_{\text{FWHM}}$ | Reference |
|---------------------------|------------------|--------------------------------------|------------|----------------------|--------------------------|-----------|
| MnCoGe                   | 1                | 1.24                                 | 281        | 38.44                | 31                       | This work |
|                           | 1.5              | 1.64                                 | 281        | 60.68                | 37                       |           |
| MnCoGe$_{0.99}$La$_{0.01}$| 1                | 1.13                                 | 279        | 36.16                | 32                       | This work |
|                           | 1.5              | 1.52                                 | 279        | 59.28                | 39                       |           |
| MnCoGe$_{0.97}$La$_{0.03}$| 1                | 1.16                                 | 279        | 34.80                | 30                       | This work |
|                           | 1.5              | 1.56                                 | 279        | 57.72                | 37                       |           |
| MnCoGe$_{0.5}$Si$_{0.5}$  | 5                | 4.4                                  | 373        | 282                  | 96                       | [34]      |
| Mn$_{0.97}$Fe$_{0.03}$CoGe | 5                | 9                                    | 276        | 221                  | 31                       | [35]      |
| Mn$_{0.96}$Fe$_{0.04}$CoGe | 5                | 5                                    | 247        | 261                  | 28                       | [35]      |
| Gd$_5$Si$_2$Ge$_2$        | 5                | 5.8                                  | 300        | 305                  | /                        | [36]      |

4. Conclusions

In this work, MnCoGe$_{1-x}$La$_x$ ($x = 0$, 0.01, 0.03) series alloys are all in the high-temperature Ni$_2$In-type MnCoGe phase. In MnCoGe$_{1-x}$La$_x$, the lattice constant gradually increases and the unit cell volume becomes larger with an increase in doped La content.
The magnetic properties of MnCoGe\textsubscript{1−x}La\textsubscript{x} series alloys were systematically studied, and we found that MnCoGe\textsubscript{1−x}La\textsubscript{x} is ferromagnetic at low temperatures and paramagnetic at room temperature. With an increase in doped content, the T\textsubscript{C} decreased and the T\textsubscript{C} of the MnCoGe\textsubscript{1−x}La\textsubscript{x} series alloys were 294, 281, and 278 K, respectively. With an increase in doped La content, the saturation magnetization at 80 K decreased slightly; being 88.75 emu/g for MnCoG, 87.55 emu/g for MnCoGe\textsubscript{0.99}La\textsubscript{0.01}, and 80.91 emu/g for MnCoGe\textsubscript{0.97}La\textsubscript{0.03} at 5K. The maximum magnetic entropy changes in MnCoGe\textsubscript{1−x}La\textsubscript{x} series alloys at |\Delta S|\textsubscript{max} = 1.5T were 1.64, 1.52, and 1.56 J·kg\textsuperscript{-1}·K\textsuperscript{-1}, respectively, and the refrigeration capacities (RC) were 60.68, 59.28, and 57.72 J·kg\textsuperscript{-1}, respectively, with a slight decrease along the series. These changes can be observed in our study, the findings of which can serve as a reference for future research into the application of rare earth element-doped MnCoGe series alloys in magnetic refrigeration.

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**References**

1. Xu, G.Z.; Liu, E.K.; Du, Y.; Li, G.J.; Liu, G.D.; Wang, W.H.; Wu, G.H. A New Spin Gapless Semiconductors Family: Quaternary Heusler Compounds. *Europhys. Lett.* 2013, 102, 17007. [CrossRef]
2. Bazela, W.; Szytula, A.; Todorovic, J.; Tomkowicz, Z.; Zięba, A. Crystal and magnetic structure of NiMnGe. *Phys. Status Solidi* 2010, R381. [CrossRef]
3. Koyama, K.; Sakai, M.; Kanomata, T.; Watanabe, K. Field-Induced Martensitic Transformation in New Ferromagnetic Shape Memory Compound Mn\textsubscript{1.02}CoGe\textsubscript{0.98}. *Jpn. J. Appl. Phys.* 2004, 43, 8036–8039. [CrossRef]
4. Caron, L.; Trung, N.T.; Brück, E. Pressure-tuned magnetocaloric effect in Mn\textsubscript{0.95}CoGe\textsubscript{0.05} alloys. *Appl. Phys. Lett.* 2011, 100, 9703. [CrossRef]
5. Liu, E.K.; Zhu, W.; Feng, L.; Chen, J.L.; Wang, W.H.; Wu, G.H.; Liu, H.Y.; Meng, F.B.; Luo, H.Z.; Li, Y.X. Vacancy-tuned paramagnetic/ferromagnetic martensitic transformation in Mn-poor Mn\textsubscript{1−x}CoGe alloys. *Europhys. Lett.* 2010, 91, 17003. [CrossRef]
6. Niziol, S.; Binczycka, H.; Szytula, A.; Todorović, J.; Fruchart, R.; Senator, J.P.; Fruchart, D. Structure magnetique des MnCoSi. *Phys. Status Solidi* 2010, 45, 591–597. [CrossRef]
7. Trung, N.T.; Zhang, L.; Caron, L.; Buschow, K.H.J.; Brück, E. Giant magnetocaloric effects by tailoring the phase transitions. *Appl. Phys. Lett.* 2010, 96, R381. [CrossRef]
8. Gbara, P.; Niadecki, Z. Structure, magnetocaloric properties and thermodynamic modeling of enthalpies of formation of (Mn,X)-Co-Ge (X = Zr, Pd) alloys. *J. Alloys Compd.* 2019, 796, 153–159. [CrossRef]
9. Kanomata, T.; Ishigaki, H.; Suzuki, T.; Yoshida, H.; Abe, S.; Kaneko, T. Magneto-volume effect of MnCo\textsubscript{1−x}Ge (0 ≤ x ≤ 0.2). *J. Magn. Magn. Mater.* 1995, 140, 131–132. [CrossRef]
16. Wang, J.T.; Wang, D.S.; Chen, C.; Nashima, O.; Kanomata, T.; Mizuseki, H.; Kawazoe, Y. Vacancy induced structural and magnetic transition in MnCo_{1-x}Ge. *Appl. Phys. Lett.* 2006, 89, 1187. [CrossRef]

17. Hassan, N.U.; Chen, F.; Zhang, M.; Shah, I.A.; Liu, J.; Gong, Y.; Xu, G.; Xu, F. Realisation of magnetostructural coupling and a large magnetic calorific effect in the MnCoGe_{1-x} system. *J. Magn. Magn. Mater.* 2017, 439, 120–125. [CrossRef]

18. Niziol, S.; Zie Ba, A.; Zach, R.; Baj, M.; Dnowski, L. Structural and magnetic phase transitions in Co_{x}Ni_{1-x}MnGe system under pressure. *J. Magn. Magn. Mater.* 1983, 38, 205–213. [CrossRef]

19. Yue, S.; Bruno, N.M.; Emre, B.; Karaman, I. Accessibility investigation of large magnetic entropy change in CoMn_{1-x}Fe_{x}Ge. *J. Appl. Phys.* 2016, 119, 622–655. [CrossRef]

20. Trung, N.T.; Biharie, V.; Zhang, L.; Caron, L.; Buschow, K.H.J.; Brück, E. From single-to double-first-order magnetic phase transition in magnetocaloric Mn_{1-x}Cr_{x}CoGe compounds. *Appl. Phys. Lett.* 2010, 96, 162507. [CrossRef]

21. Bao, L.F.; Huang, W.D.; Ren, Y.J. Tuning Martensitic Phase Transition by Non-Magnetic Atom Vacancy in MnCoGe Alloys and Related Giant Magnetcataloric Effect. *Chin. Phys. Lett.* 2016, 33, 077502. [CrossRef]

22. Yuan, Z.M.; He, J.; Yang, L.; Xia, Z.J.; Zhao, D.L.; You, C.Y.; Ren, W.J. Influence of microstructural changes on magnetic refrigeration performance for La(Fe_{0.94}Co_{0.06})_{11.8}Si_{1.2} alloys during magnetic field cycling. *J. Appl. Phys.* 2015, 117, 162406. [CrossRef]

23. Chen, X.; Chen, Y.G.; Tang, Y.B.; Xiao, D.Q. 1:13 phase formation mechanism and first-order magnetic transition strengthening characteristics in (La, Ce)Fe_{13-x}Si_{x} alloys. *Rare Met.* 2016, 36, 33–42.

24. Guchowski, P.; Nikonkov, R.; Tomala, R.; Stręk, W.; Shulha, T.; Serdechnova, M.; Zheleudkevich, M.; Pakalaniškis, A.; Skaudžius, R.; Kareiva, A.; et al. Magnetic Properties of La_{0.9}A_{0.1}MnO_{3} (A: Li, Na, K) Nanopowders and Nanoceramics. *Materials 2020*, 13, 1788. [CrossRef][PubMed]

25. Botello-Zubiate, M.; Grijalva-Castillo, M.; Soto-Parra, D.; Sáenz-Hernández, R.J.; Santillán-Rodriguez, C.R.; Matutes-Aquino, J.A. Preparation of La_{0.7C_{0.3-x}}Sr_{x}MnO_{3} Manganites by Four Synthesis Methods and Their Influence on the Magnetic Properties and Relative Cooling Power. *Materials 2019*, 12, 309. [CrossRef]

26. Fang, Y.K.; Yeh, C.C.; Chang, C.W.; Chang, W.C.; Zhu, M.G.; Li, W. Large low-field magnetocaloric effect in MnCo_{0.95}Ge_{1.14} alloy. *Scr. Mater.* 2007, 57, 453–456. [CrossRef]

27. Jeitschko, W. A high-temperature X-ray study of the displacive phase transition in MnCoGe. *Acta Crystallograph. Sect. B Struct. Ence 2010*, 61, 1187–1190. [CrossRef]

28. Wu, X.; He, W.; Yang, T.; Xiao, G.; Chen, P.; Bi, Y.; Wu, W. The magnetic and electronic properties of REAgSb_{3} compounds. *J. Magn. Magn. Mater.* 2021, 519, 167442. [CrossRef]

29. Zhao, F.Q.; Dagula, W.; Tegus, O.; Buschow, K.H.I. Magnetic-entropy change in Mn_{0.7}Ge_{3-x}Si_{x} alloys. *J. Alloys Compounds 2006*, 416, 43–45. [CrossRef]

30. Banerjee, B.K. On a generalised approach to first and second order magnetic transitions. *Phys. Lett.* 1964, 12, 16–17. [CrossRef]

31. Zhang, D.; Nie, Z.; Wang, Z.; Huang, L.; Zhang, Q.; Wang, Y.D. Giant magnetocaloric effect in MnCoGe with minimal Ga substitution. *J. Magn. Magn. Mater.* 2015, 387, 107–110. [CrossRef]

32. Bao, L.F.; Hu, F.X.; Wu, R.R.; Wang, J.; Chen, L.; Sun, J.R.; Shen, B.G.; Li, L.; Zhang, B.; Zhang, X.X. Evolution of magnetostructural transition and magnetocaloric effect with Al doping in MnCoGe_{1-x}Al_{x} compounds. *J. Phys. Appl. Phys.* 2014, 47, 1–7. [CrossRef]

33. Si, X.; Shen, Y.; Ma, X.; Chen, S.; Lin, J.; Yang, J.; Gao, T.; Liu, Y. Field dependence of magnetic entropy change and estimation of spontaneous magnetization in Cd substituted MnCoGe. *Acta Mater.* 2017, 143, 306–317. [CrossRef]

34. Choudhury, D.; Suzuki, T.; Tokura, Y.; Taguchi, Y. Tuning structural instability towards enhanced magnetocaloric effect around room temperature in MnCo_{0.5}Zn_{0.5}Ge. *Sci. Rep.* 2014, 4, 7544. [CrossRef][PubMed]

35. Ren, Q.Y.; Hutchison, W.D.; Wang, J.L.; Studer, A.J.; Din, M.M.; Pérez, S.M.; Cadogan, J.M.; Campbell, S.J. The magneto-structural transition in Mn_{1-x}Fe_{x}CoGe. *J. Phys. D Appl. Phys.* 2016, 49, 175003. [CrossRef]

36. Provenzano, V.; Shapiro, A.J.; Shull, R.D. Reduction of hysteresis losses in the magnetic refrigerant Gd_{5}Ge_{2}Si_{2} by the addition of iron. *Nature 2004*, 429, 853. [CrossRef]