Observation and analysis of Fano-like lineshapes in the Raman spectra of molecules adsorbed at metal interfaces

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Surface-enhanced Raman scattering (SERS) from bipyridyl ethylene adsorbed on gold dumbbells shows Fano-like spectra at high incident light intensity. This is accompanied by an increased electronic temperature, while no vibrational anti-Stokes scattering is observed. Theory indicates that interference between vibrational and electronic Raman scattering can yield such asymmetric scattering lineshapes. The best fit to observations is however obtained by disregarding this coupling and accounting for the detailed lineshape of the continuous electronic component of the SERS.

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I. INTRODUCTION

The surface-enhanced optical response of molecules adsorbed on metal surfaces reflects the effect of strong local fields created by surface plasmons [1–3] as well as charge transfer between the molecule and metal [4–7]. Surface-enhanced Raman scattering (SERS) has become an important diagnostic tool for molecules at metallic interfaces, including molecular conduction junctions [8–15]. (See also Refs. [16–27] for related theoretical work.) At metal interfaces, vibrational Raman scattering is accompanied by a continuous background resulting from inelastic contributions of electron-hole (e-h) excitations in the metal [1,4,28–30]. Both components of the inelastic scattering signal were recently used to determine the bias-induced heating in a molecular conduction junction [13].

While it is generally recognized that the electronic background is affected by the molecule-substrate interaction, these two components of the SERS signal are usually treated separately. Surprisingly, we observe (Fig. 1) an apparent Fano-like feature in the Raman spectra from the same system, bipyridyl ethylene adsorbed on gold nanosphere dimers (dumbbells), that may indicate interference between these two scattering channels. Below we discuss the origin of this observation. It should be noted that Fano-like profiles were previously observed [31] in the surface-enhanced femtosecond stimulated Raman spectra of the same system as in the present study: bipyridyl ethylene (BPE) molecules adsorbed on gold nanosphere dimers (dumbbells). This observation was attributed to interference between the vibrational coherence generated by the combined action of pump and probe pulses and plasmons excited in the metal structure. However, no detailed mechanism was offered. Such a mechanism should also account for the observed absence of interference effects in the normal Raman scattering from the same system and for the fact that, while coupling between vibrations and metal is needed to account for such interference, no effect of the proximity to the metal on the vibrational decoherence rate could be detected.

The measurements are carried out on single silica-encapsulated gold dumbbells (Fig. 1, left inset). The nanosphere diameter is $95 \pm 5$ nm, and the intersphere spacing prior to irradiation is $\sim 1$ nm. On these dumbbells, the quadrupolar and the binding dipolar plasmon resonances occur near 560 and 780 nm, respectively [32]. As a molecular reporter, BPE is adsorbed on the gold spheres prior to encapsulation. The dumbbells are dispersed on a silicon nitride membrane (20 nm thick) of a TEM grid by drop casting them in a dilute solution. Locations and geometries of the nanostructures are mapped using a scanning electron microscope (SEM); then Raman scattering measurements are done under an optical microscope, in the backscattering geometry, using an objective with a numerical aperture (NA) of 0.625. The excitation source is a continuous-wave diode laser, operating at $\lambda = 532$ nm, coincident with the antibonding quadrupolar surface plasmon resonance [32]. The molecular vibrational Raman spectra appear over a background continuum [Fig. 1, line (b)], which is also seen on bare dumbbells [Fig. 1, line (a)]. As discussed before [33], at low intensity, $10 \mu W/\mu m^2$, the vibrational spectrum is not affected by the proximity to the metal (in agreement with Ref. [31]) and matches that of the isolated BPE molecule. Two observations are most significant at higher incident intensities: (a) The molecular lines broaden asymmetrically to eventually coalesce into the single asymmetric profile, similar to a Fano-type lineshape [Fig. 1, lines (c) and (d)]. (b) The electronic and vibrational temperatures, $T_e$ and $T_v$, inferred from the AS branch of the electronic Raman scattering (see Fig. 2) and Stokes/anti-Stokes (S/AS) intensity ratio of the vibrational Raman line appear to be different. At the highest incident light intensity $T_e$ reached 580 K, while no molecular AS scattering is seen, which would set the apparent vibrational temperature of the molecule $T_v$ to less than 300 K. More experimental details and results are presented in the Supplemental Material [34].

The central question raised by these observations is whether the lineshapes shown in Fig. 1, lines (c) and (d), are indeed interference features as their Fano-like lineshapes suggest. Specifically, can there be interference between the electronic and vibrational Raman scattering pathways that coexist in this system? The intuitive answer is negative because the two pathways lead to different final states. In contrast, in this paper...
we present theoretical models that show that such interference can happen. Our theory focuses on the generic aspects of such processes and yields two main results: (a) The aforementioned interference can exist in the presence of electron-vibration coupling and can, in principle, lead to the observed lineshapes. (b) However, comparing the detailed calculations with the available experimental observations suggests that another mechanism, asymmetric electronic sidebands dressing the molecular Raman spectrum, may be dominant in this system.

We consider two models, described in Sec. II. One of these (model A) assumes that the dominant optical interaction is intramolecular and that the effect of the metal substrate results from the molecule-metal interaction. Model B considers, in addition to the intramolecular optical processes, also optically induced molecule-metal charge transfer. Section III and the Supplemental Material describe our theoretical approach, and Sec. IV presents the results of our model calculations. Section V concludes.

II. MODELS

We consider a molecule chemisorbed on a metal surface and subjected to an external radiation field. In the experimental system the metal is a nanostructure (NS) that promotes plasmonic enhancement, but this enters our discussion only implicitly, through the magnitude of the local electromagnetic field. The model Hamiltonian comprises the molecule, metal, radiation field, and their couplings, with the electron-photon and e-v interaction terms treated as perturbations:

\[ \hat{H} = \hat{H}_0 + \hat{V}_{rad} + \hat{V}_{e-v} , \]

where \( \hbar = k_B = e = 1 \)

\[ \hat{H}_0 = \hat{H}_M + \hat{H}_NS + \hat{V}_NS + \hat{H}_{rad} , \]

\[ \hat{H}_M = \sum_{m=g,x} \epsilon_m \hat{a}_m \hat{a}_m^\dagger + \omega_v \hat{v} \hat{v}^\dagger , \]

\[ \hat{H}_{NS} = \sum_k \epsilon_k \hat{c}_k \hat{c}_k^\dagger , \]

\[ \hat{V}_{NS} = \sum_{m=g,x} \sum_k (V_{mk} \hat{d}_m^\dagger \hat{c}_k + V_{km} \hat{c}_k^\dagger \hat{d}_m) , \]

\[ \hat{V}_{e-v} = \sum_{m=g,x} M_m \hat{Q}_m \hat{a}_m^\dagger \hat{a}_m , \]

\[ \hat{V}_{rad} = \sum_{a \in \{f\}} \hat{v}_a \hat{\alpha}_a^\dagger \hat{\alpha}_a , \]

\[ \hat{M}_M = \text{the molecular Hamiltonian, modeled as a two-electronic-level (ground and excited states, g and x) system with a single molecular vibration of frequency } \omega_v . \hat{V}_{e-v} \text{ is the corresponding polaronic-type e-v coupling. } \hat{H}_{NS} \text{ describes a}

\[ \hat{V}_{rad} = \hat{V}_{rad}^C + \hat{V}_{rad}^M \]

\[ = \sum_{J=C,M} \sum_{a \in \{f\}} \left( U_{gs,a}^J (\hat{Q}_x) \hat{D}_j \hat{\alpha}_a + U_{ag,x}^J (\hat{Q}_g) \hat{\alpha}_a^\dagger \hat{D}_j \right) . \]
free-electron metal, and \( \hat{V}_{\text{NS}} \) is the molecule-metal electron transfer coupling. \( \hat{d}_m^\dagger \) \((\hat{d}_m); m = g, x) \) and \( \epsilon_k^\dagger \) \((\epsilon_k) \) create (annihilate) electrons in the molecular orbitals and the metal, respectively. \( \hat{V}_\text{C} \) \((\hat{v}_\text{C}) \) and \( \hat{d}_k^\dagger \) \((\hat{d}_k); g \) create (annihilate) vibrational excitations and photons in mode \( \alpha \), respectively. Finally, \( \hat{D}_M = \hat{d}_M^\dagger \hat{d}_a \) and \( \hat{D}_C = \hat{d}_C^\dagger \hat{c}_k \) are, respectively, intramolecular and charge-transfer electronic deexcitation operators. \( \hat{V}_\text{rad} \) \( Eq. (8) \) is the system-radiation-field coupling in which the coupling matrix elements \( U^J_{g,x,\alpha} \) connect the molecular ground state \( g \) to electronically excited states \( x \). The channel index \( J = \{M, C\} \) corresponds to the nature of the excited states \( x \): excited molecular states in channel \( M \) and excited metal states in channel \( C \). [We have disregarded a term similar to \( (8) \) but with the lower-energy state belonging to the pure metal that is associated with light scattering from the bare metal but does not contribute to the interference mechanism discussed below.]

As usual, we distinguish between the incoming (occupied) photon mode \( i \) and the continuum of accepting (empty) modes \( \{f\} \). These coupling elements are assumed to be functions of the vibrational coordinate, described here by their Taylor expansion up to the linear term \( J = \{M, C\} \)

\[
U^J_{g,x,\alpha}(\hat{Q}_e) \equiv U^J_{g,x,\alpha}^{(s)}(\hat{Q}_e) \approx U^{(0)}_{g,x,\alpha} + U^{(1)}_{g,x,\alpha} \hat{Q}_e.
\]

To account for the observed dependence of the inelastic spectrum on the incident light intensity, we assume that in addition to being scattered, the incident radiation field affects the molecule-metal coupling. This can arise from a field-induced renormalization of the electron transfer coupling \( \hat{V}_\text{NS} \). \( Eq. (5) \) \([35–37]\), as well as contributions from molecule-to-metal charge-transfer transitions. In the calculations reported below this is incorporated by an assumed dependence of the self-energies \( \Gamma_m \) \((m = g, x) \) on the incident light intensity.

### III. THEORETICAL CONSIDERATIONS

Consider first model A [Fig. 3(a)]. Here we assume that Raman scattering is dominated by the intramolecular optical transition and disregard the corresponding contribution of the optical charge transfer coupling \( \hat{V}_\text{C} \). This model can show interference between the vibrational and electronic scattering channels, provided that their coupling, \( Eq. (6) \), is strong enough.

Following the procedure described in Ref. [18], the (normal) Raman scattering flux \([38]\) has the following structure:

\[
J_{i \rightarrow f}^{(1)} = \int_{-\infty}^{0} d(t'-t) \int_{-\infty}^{0} d(t_1-t) \int_{-\infty}^{0} d(t_2-t')
\times e^{-i\phi(t'-t)} e^{-i\phi(t_1-t)}
\times (\hat{U}_i(t_2) \hat{D}_i(t_2) \hat{U}_f(t') \hat{D}_f(t') \hat{U}_f(t) \hat{D}_f(t_1)) \hat{U}_f(t_1) \hat{D}_f(t_1)),
\]

in which the operators are summed over all relevant contributions from Eqs. (8) and (9) and where the indices \( i \) and \( f \) indicate that the corresponding matrix element should be taken with the incident or scattered radiation field modes, respectively. In a departure from Ref. [18] we keep only the lowest order (up to second) terms in \( U^J \), as is usually done for nonresonant Raman calculations. The calculation proceeds as follows (see the Supplemental Material for details):

(a) Applying \( Eq. (10) \) to model A yields Eqs. (S2) for the light-scattering flux. Expressions (S2b)–(S2e) formally represent interference between vibrational and electronic Raman/Rayleigh scattering. At the level of the present calculation, fourth order in the coupling to the radiation field, they vanish in the absence of the coupling (6).

(b) The \( e-v \) interaction (6) is considered to the lowest order.

This introduces an additional term, \( \int d\tau_c \hat{M}_C \hat{Q}_e(\tau_c) \hat{h}_s(\tau_c) \), into the correlation functions (S2b)–(S2e), yielding nonvanishing corrections that represent interference between the electronic and vibrational Raman processes. These corrections give nonvanishing contributions to the interference terms, Eqs. (S2b)–(S2e), which can give rise to a Fano lineshape in the Raman scattering, as shown below [39].

(c) The light-scattering flux including the interference corrections is thus obtained in terms of correlation functions of a system defined by the quadratic Hamiltonian \( \hat{H}_0 \). Consequently, Wick’s theorem applies, and electronic and vibrational degrees of freedom decouple, yielding the final expressions in terms of projections of the electronic and vibrational Green’s functions, Eqs. (S5)–(S9).

This procedure leads to an explicit expression for the light-scattering flux as a sum over several contributions, \( J_{i \rightarrow f} = J_{i \rightarrow f}^{(1)} + J_{i \rightarrow f}^{(2)} + J_{i \rightarrow f}^{(3)} + J_{i \rightarrow f}^{(4)} \), where \( J_{i \rightarrow f}^{(1)} \) is the electronic Raman flux and \( J_{i \rightarrow f}^{(2)} \) is the correction to this flux due to the electron-vibration coupling. Similarly, \( J_{i \rightarrow f}^{(3)} \) and \( J_{i \rightarrow f}^{(4)} \) are, respectively, the vibrational Raman flux and the correction.
to this flux associated with the electron-vibration coupling. Explicit expressions for these contributions are given by Eqs. (S10)–(S16).

We have also considered model B as an alternative mechanism for interference. The calculation follows the same steps as in (a) and (c) above, now using both $M$ and $C$ terms in Eq. (8). In this calculation we have restricted our considerations to contributions from the purely intramolecular processes [$D = D_M$ in all four terms in (10)], purely charge-transfer processes ($D = D_C$ in all terms), and their mixtures (potential source of interference) in which excitation operators at times $t_2$ and $t'_2$ are of one kind, while those at times $t$ and $t_1$ are of the other. The final result for the light-scattering flux for this model is given by Eqs. (S17)–(S21).

IV. RESULTS

Figure 4 shows the total Raman scattering signal resulting from a calculation based on model A and on a reasonable choice of molecular parameters. The calculation was done on an energy grid spanning the region from $-3$ to $3$ eV with a step of $10^{-3}$ eV, and the molecular vibration is assumed to equilibrate quickly to the ambient temperature. The following observations can be made:

(a) Interference between electronic and vibrational inelastic scattering routes can indeed lead to a Fano-type scattering spectrum. The electron-vibration coupling (6) is crucial for obtaining this behavior. This is seen in the weak-illumination case [Fig. 4(a)] by comparing the results obtained with and without this coupling.

(b) The asymmetric lineshape that is seen in the high-incident-intensity case [Fig. 4(b)] is not of this origin. In this case the calculation yields Fano-like lineshapes that qualitatively reproduce the experimental behavior also when the coupling (6) is disregarded.

(c) Our analysis thus shows that interference between vibrational and electronic Raman scattering can, in principle, lead to a characteristic Fano lineshape in Raman scattering from molecules at metal interfaces. The origin of the present observation appears, however, to be different, resulting from the Stokes component of the electronic Raman scattering. Indeed, Fig. 5(a) shows that the asymmetry disappears at high ambient temperatures.

Our calculation also yields the effective (Raman) temperature from the ratio between the S and AS scattering intensities according to [13,17,18] $T_{\text{eff}}^{(1)} = \frac{\text{S}}{\text{AS}} = \frac{\Delta T}{\Delta s} = \frac{\Delta T}{\Delta s}$, or fitting the tail of the AS signal to $a \Delta T/(1 - \exp[(-\Delta T)/T_{\text{eff}}^{(2)})]$.  

\[ T_{\text{eff}}^{(1)} = \frac{\text{S}}{\text{AS}} \]

\[ T_{\text{eff}}^{(2)} = \frac{\Delta T}{\Delta s} \]

\[ a \Delta T/(1 - \exp[(-\Delta T)/T_{\text{eff}}^{(2)})] \]
We have observed asymmetric lineshape features in Raman scattering from bipyridyl ethylene molecules adsorbed on gold nanostructures, with the following characteristics: (a) Asymmetry increases with incident light intensity. (b) The vibrational temperature appears not to increase even at the highest intensity used, while the apparent electronic temperature increases by up to \( \sim 600 \) K. The Fano-like appearance of these lineshapes suggests the possible implication of interference between different scattering pathways. Model calculations show that such interference, leading to the observed asymmetry, is indeed possible in systems with strong enough electronic-vibrational coupling. Our calculations suggest, however, that the observed lineshape asymmetry is dominated by electronic scattering sidebands that dress the Rayleigh and vibrational scattering peaks, and its dependence on incident light intensity can be explained by an optically induced component in the molecule-metal electron-transfer coupling. This model also yields vibrational and electronic “Raman temperatures” that are consistent with experimental observation but may reflect the complex nature of the nonequilibrium response rather than the actual temperature. Fano-type interference in Raman scattering has been shown to be a theoretical possibility.

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[38] We limit consideration to unbiased or weakly biased junctions, where only normal Raman scattering, for which the initial electronic state is the ground state of the molecule, can take place.
[39] A closer look at the details of these corrections reveals that corrections to (S2b)–(S2c) from projections (e)–(h) of Fig. S5 and corrections to (S2d)–(S2e) from projections (a)–(d) of Fig. S5 represent renormalization of the electronic Raman signal due to e-v interaction. These terms dominate the resulting Fano resonance that is seen in the calculated Raman scattering at low incident light intensity [inset to Fig. 3(a)]. Corrections to (S2b)–(S2c) from projections (a)–(d) of Fig. S5 and corrections to (S2d)–(S2e) from projections (e)–(h) of Fig. S5 lead to renormalization of the vibrational Raman scattering and are also included in the calculations reported here.
[40] For $T_{\text{eff}}^{(1)}$ we have arbitrarily assigned the vibrational Raman temperature to the value calculated at $\Delta \nu = \omega_v$ and the electronic Raman temperature to that obtained at $\Delta \nu = 2\omega_v$. 
