A novel logistic regression model combining semi-supervised learning and active learning for disease classification

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Traditional supervised learning classifier needs a lot of labeled samples to achieve good performance, however in many biological datasets there is only a small size of labeled samples and the remaining samples are unlabeled. Labeling these unlabeled samples manually is difficult or expensive. Technologies such as active learning and semi-supervised learning have been proposed to utilize the unlabeled samples for improving the model performance. However in active learning the model suffers from being short-sighted or biased and some manual workload is still needed. The semi-supervised learning methods are easy to be affected by the noisy samples. In this paper we propose a novel logistic regression model based on complementarity of active learning and semi-supervised learning, for utilizing the unlabeled samples with least cost to improve the disease classification accuracy. In addition to that, an update pseudo-labeled samples mechanism is designed to reduce the false pseudo-labeled samples. The experiment results show that this new model can achieve better performances compared the widely used semi-supervised learning and active learning methods in disease classification and gene selection.

Identifying disease related genes and classifying the disease type using gene expression data is a very hot topic in machine learning. Many different models such as logistic regression model and support vector machines (SVM) have been applied in this area. However these supervised learning methods need a lot of labeled samples to achieve satisfactory results. Nevertheless in many biological datasets there is only a small size labeled data and remaining samples are unlabeled. Labeling these unlabeled samples manually is difficult or expensive; hence many unlabeled samples are left in the dataset. On the other hand, the proportion of small size labeled samples may not represent the real data distribution, which makes the classifier difficult to get the expected accuracy. Trying to improve the classification performance, many incrementally learning technologies such as semi-supervised learning (SSL) and active learning (AL) have been designed which utilize the unlabeled samples.

AL tries to train an accurate prediction model with minimum cost of labeling the unlabeled samples manually. It selects most uncertain or informative unlabeled samples and annotates them by human experts. These labeled samples are included to the training dataset to improve the model performance. Nevertheless in many biological datasets there is only a small size labeled data and remaining samples are unlabeled. Labeling these unlabeled samples manually is difficult or expensive; hence many unlabeled samples are left in the dataset. On the other hand, the proportion of small size labeled samples may not represent the real data distribution, which makes the classifier difficult to get the expected accuracy. Trying to improve the classification performance, many incrementally learning technologies such as semi-supervised learning (SSL) and active learning (AL) have been designed which utilize the unlabeled samples.

In another way, SSL uses unlabeled data together with labeled data in the training process without any manual labeling. Many different SSL methods have been designed in machine learning including transductive support vector machines, graph-based methods, co-training, self-training and so on. However pointed out that the pseudo-labeled samples are annotated based on the labeled samples in the dataset, and they are easy to be affected by the noisy samples. That is why SSL may not achieve satisfactory accuracy in some places.

Many researchers found the complementarity between AL and SSL. Song combined the AL and SSL to extract protein interaction sentences, the most informative samples which were selected by AL-SVM were annotated by...
experts and then the classifier was retrained using SSL technology by the new dataset\(^1\). used a SSL technology to help AL select the query points more efficiently and further reducing the workload of manual classification. In\(^1\) a SVM classifier was proposed to manually label the most uncertain samples and at the same time the other unlabelled samples were labeled by SSL, thus a faster convergence result was gained. The recent study\(^1\) proposed by Lin designed a new active self-paced learning mechanism which combines the AL and SSL for face recognition.

However, most attention of the methods combining SSL and AL are paid to the SVM model. The logistic regression model which widely used for disease classification is seldom mentioned. And also in these existing methods, the most informative samples selected by AL are manually annotated, this work maybe very expensive or time consuming in disease classification. Hence we design a new logistic regression model combining AL and SSL which meets the following requirements:

The new model should be easily understood and applied. Our method should not require significant engineering overhead to use.

In this new logistic regression model, we use uncertainty sampling to select the most informative samples in AL. Uncertainty sampling is fairly easily generalized to probabilistic structure prediction models. For logistic regression model, the sample probability closed to the decision boundary (probability \(\approx 0.5\)) will suffice. In the new logistic regression model, self-training is used as a complement to AL. Self-training is one of the popular technologies used in SSL because of its fast speed and simplicity, and this method is a good way to solve the short-sighted problem in AL. In self-training the classifier is first trained by using the small size labeled samples, and then the obtained classifier will be used to label the high confidence samples in the unlabeled samples pool. These selected samples will be included into the training set and the classifier will be retrained. The cycle repeats until all the unlabeled samples have been used. In the logistic regression model, the samples which the probability closed to 0 or 1 can be seen as the high confidence samples were labeled by SSL, thus a faster convergence result was gained. The recent study\(^1\) proposed by Lin designed a new active self-paced learning mechanism which combines the AL and SSL for face recognition.

The new model can achieve a satisfactory accuracy while labeling the samples automatically without manual labeling.

Sometimes labeling the disease samples manually is difficult, expensive or time consuming. In our model the uncertain samples selected by AL are labeled by the last classifier automatically, it significantly reduces the burden of manual labeling. However how to ensure the correctness of these uncertain samples? The most uncertain samples mean the false pseudo-labeled samples are easy to be generated. On the other hand the most uncertain samples can be seen as the most informative samples in the logistic model, and the misclassified samples will degenerate the model performance obviously. Considering these samples are not removed or corrected in the standard AL and SSL methods, we design an update mechanism for the pseudo-labeled samples which makes the misclassified samples have chances to be corrected based on the new classifiers which generated in later training interactions.

Method

Logistic regression model. Supposing the biological dataset has \(n\) samples, which includes \(n_1\) labeled samples and \(n_2\) unlabeled samples, \(n=n_1+n_2\). And this dataset contains \(p\) genes. \(\beta\) (\(\beta = \beta_0 + \beta_1 + \beta_2 + \ldots + \beta_p\)) represents the coefficients between the disease type Y and gene expression \(X_\text{gene}\). \(X_\text{gene}\) represents the individual sample, where \(y_i\) is disease type, \(x_i = (x_{i1}, x_{i2}, \ldots, x_{ip})\) represents the gene expression data, \(c_i\) represents the sample is labeled or unlabeled. The basic logistic regression model can be expressed as:

\[
P(y_i = 1|x_i) = \frac{\exp(x_i\beta)}{1 + \exp(x_i\beta)}
\]

The log-likelihood of the logistic regression method can be expressed as:

\[
\ell(\beta) = -\sum_{i=1}^{n_1} y_i \log \left( \frac{\exp(x_i\beta)}{1 + \exp(x_i\beta)} \right) + (1 - y_i) \log \left( \frac{1 + \exp(x_i\beta)}{1 + \exp(x_i\beta)} \right)
\]

Trying to identify disease related genes in the gene expression data, L1-norm regularization (Lasso) is added in the model:

\[
\min \sum_{i=1}^{n_1} l(x_i^T, y_i, \beta) + \lambda P(\beta)
\]

Where \(P(\beta)\) is the L1-norm regularization part and \(\lambda\) is the tuning parameter.

Uncertainty sampling. In the active learning part of our method, we use uncertainty sampling to select samples in the unlabeled dataset. In the logistic regression model the sample which probability close to the decision boundary (probability \(\approx 0.5\)) can be seen as the most uncertain sample in AL. Hence an AL logistic regression model can be expressed as:

\[
\min \sum_{i=1}^{n_1} l(x_i^T, y_i, \beta) + \sum_{j=1}^{n_2} y_j f_{\text{AL}}(\beta) + \lambda P(\beta)
\]
where \( v \) is the weight parameter of the unlabeled samples, and the \( f_{AL}(v, \alpha) \) represents the selection function which can be used to generate the \( v, \alpha \) is the control parameter. The selected unlabeled samples will be labeled manually and then included into the training dataset. The \( f_{AL}(v, \alpha) \) can be expressed as following:

\[
v_j = \begin{cases} 
1 & 0.5 - \alpha < \ell(x_j^T, \beta) < 0.5 + \alpha \\
0 & \text{else}
\end{cases}
\]

**Self-training.** In the logistic regression model the sample probability closest to 0 or 1 can be seen as the high confidence sample. It is easy to find that the difference between the self-training and uncertainty sampling is that the selection criteria of identifying the used unlabeled samples. Hence the self-training logistic regression model is shown as:

\[
\min \sum_{i=1}^{n_1} l(x_i^T, \beta) + \sum_{j=1}^{n_2} w_j l(x_j^T, \beta) + f_{SSL}(w_j, \gamma) + \lambda P(\beta)
\]

where \( w \) is the weight parameter of the unlabeled samples, the \( f_{SSL}(w, \gamma) \) represents the selection function of self-training and \( \gamma \) is the control parameter. The \( f_{SSL}(w, \gamma) \) is shown as:

\[
w_j = \begin{cases} 
0 & \gamma < \ell(x_j^T, \beta) < 1 - \gamma \\
1 & \text{else}
\end{cases}
\]

**The logistic regression model combining semi-supervised learning and active learning.** In this paper we propose a novel logistic regression model combining SSL and AL with an update mechanism. The high confidence unlabeled samples selected by self-training can avoid the classifier to be short-sighted. The low confidence samples selected by uncertainty sampling prevent the classifier to be misled by high noisy samples which are offered by self-training. The model can be expressed as:

\[
\min \sum_{i=1}^{n_1} w_i l(x_i^T, \beta) + \sum_{j=1}^{n_2} (w_j \oplus v_j) l(x_j^T, \beta) + f_{AL}(v_j, \alpha) + f_{SSL}(w_j, \gamma) + \lambda P(\beta)
\]

where \( w \) is the weight parameter of the unlabeled samples given by SSL, and the \( v \) is the weight parameter of the unlabeled samples obtained by AL.

Different from the ordinary AL methods, the unlabeled samples selected in our model are labeled by the learned classifier automatically. Considering the uncertainty of classified samples, the misclassified samples should have the chances to be revised in later training iterations. The update mechanism is described below:

- If the sample is selected by SSL and the label has been changed by the classifier, this sample will be returned to the unlabeled sample pool and wait to be selected again.

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**Figure 1.** The work flow of proposed logistic regression model combining SSL and AL.
If the sample is selected by AL and the label has been changed, we revise the label of this sample and it will be put into the training dataset directly.

The work flow of our proposed logistic regression model is show in Fig. 1:

- Step 1: Firstly the labeled data will be used to learn an initial logistic regression model.
- Step 2: The logistic regression model will be used to label the unlabeled samples and the high value samples which are selected by SSL or AL will be included into the training dataset.
- Step 3: Update the logistic regression model using the new training dataset.
- Step 4: Identify the false pseudo-labeled samples. If they are selected by SSL, return them to the unlabeled sample pool. Otherwise, change their labels and put them into the training dataset directly.
- Step 5: The cycle will continue until all the unlabeled samples have been labeled or the run time exceeds the maximum number of iteration.

Algorithm 1. The algorithm of the semi-supervised logistic regression model.

**Input:** The labeled dataset $N_1$, unlabeled dataset $N_2$, maximum iteration $C$

**Output:** Model coefficient $\beta$

1: Initialize the importance weights $v$, $w$, pseudo-labeled sample set $N_3$
2: Set training dataset $N_4 = N_1$, age parameter iteration = 1
3: while not converge || iteration $\leq C$ do
4:    Learn to construct a logistic classifier based on $N_4$
5:    Label the unlabeled samples in $N_2$ automatically
6:    Build the most confidence samples set $N_{SSL}$ and most uncertain samples set $N_{AL}$
7:    if $N_3 \neq \emptyset$
8:        Estimate the pseudo-labeled samples in $N_3$
9:    end
10:   Update $N_3$ using the update mechanism
11:  Update the training dataset $N_4$ based on the $N_{AL}$, $N_{SSL}$ and $N_3$.
12:  Update the unlabeled dataset $N_2$ and pseudo-labeled sample set $N_3$
13:  Initialize $N_{AL}$, $N_{SSL}$ and $v$, $w$
14: end while
15: Return coefficient $\beta$

The algorithm of our proposed logistic regression model combining SSL and AL is given in below:

The maximum iteration $C$ is computed based on the step size $SZ$ which is the selection range for identifying high value samples based on the pseudo-labeled samples’ probabilities. The $prob_i$ is defined as the probability of the $i$th pseudo-labeled sample which is estimated by the logistic model. Here we give an example to discuss the convergence of this model: if the $SZ$ is set 0.2, the $C$ is 5 ($SZ * C = 1$). In first iteration only the pseudo-labeled samples meeting the following conditions will be used: $0 < prob_i < 0.05$ and $0.95 < prob_i < 1$ (selected by SSL) & $0.45 < prob_i < 0.55$ (selected by AL), here the initial probability range is 0.2; in the second iteration the range will be increased to $0 < prob_i < 0.1$ and $0.9 < prob_i < 1$ (selected by SSL) & $0.4 < prob_i < 0.6$ (selected by AL), the probability range is increased to 0.4, $SZ = 0.2$ means in every iteration the range of probability will increase by 0.2. And while $C = 5$, the probability range is increased to 1, it means all the pseudo-labeled samples will be used. The commonly $C$ is set $10$ ($SZ = 0.1$) or $20$ ($SZ = 0.05$). Sometimes before the iteration reaches the maximum iteration $C$, all the pseudo-labeled samples have been selected, especially while the $SZ$ is set very small. For saving the computing time and cost, the program will be terminated early.

**Results**

**Simulation experiments.** The datasets used in simulation experiments are generated as following:

- Step 1: Supposing the dataset has $n$ samples, and the number of the genes is 4000. In these 4000 genes we set 10 disease related genes, and the coefficients of the remaining 3990 genes are set zero.
- Step 2: The correlation coefficient $\rho$ is set 0.3, $x_i = \gamma_0 + \sum_{i=1}^{n} x_i \beta + \epsilon$, where $\gamma_0$, $\gamma_1$, ..., $\gamma_p$ ($i = 1, ..., n$) are generated independently from standard normal distribution
- Step 3: The sample is generated as: $\log \frac{Y_i}{1 - Y_i} = \beta_0 + \sum x_i \beta + \epsilon$, where $\beta_0$ is the intercept and $\epsilon$ is the randomly generated Gauss white noise.
Step 4: The unlabeled data points are selected randomly, supposing in the dataset there are \( n_1 \) labeled samples and \( n_2 \) unlabeled samples, where \( n = n_1 + n_2 \). In Group A we suppose \( n_1 = 100 \), \( n_2 = 200 \); and in Group B \( n_1 = 150 \), \( n_2 = 300 \). We recorded the \((y_i, x_i, c_i)\), \( c_i = 0 \) means the corresponding \( y_i \) is unlabeled.

In this paper we compare six different methods: the single logistic model with Lasso, the AL logistic model with Lasso (AL-lo), the self-training logistic model with Lasso (SSL-lo), the logistic model combining with AL and SSL which needs manual labeling (ASSL-lo), the auto logistic model with Lasso combining with AL and SSL without manual labeling and update mechanism (Auto-ASSL(A)), and the logistic model with Lasso combining with AL and SSL without manual labeling but using update mechanism (Auto-ASSL(B)). In AL-lo and ASSL-lo, about 40% unlabeled samples are labeled manually. The classification accuracy of the unlabeled data is used to evaluate the classification performances of different models. The number of selected correct genes (NC), the

|                | Group A   |        | sensitivity | specificity | Group B       |        | sensitivity | specificity |
|----------------|-----------|--------|-------------|-------------|---------------|--------|-------------|-------------|
| logistic       | 3.15      | 14.05  | 0.315       | 0.995       | 4.82          | 26.58  | 0.482       | 0.989       |
| AL-lo          | 3.65      | 17.80  | 0.365       | 0.992       | 5.19          | 28.16  | 0.519       | 0.988       |
| SSL-lo         | 3.87      | 23.61  | 0.387       | 0.990       | 5.51          | 45.40  | 0.551       | 0.979       |
| ASSL-lo        | 5.32      | 63.90  | 0.532       | 0.971       | 6.74          | 96.27  | 0.674       | 0.955       |
| Auto-ASSL(A)   | 3.59      | 57.68  | 0.359       | 0.973       | 5.26          | 97.39  | 0.526       | 0.953       |
| Auto-ASSL(B)   | 4.17      | 27.45  | 0.417       | 0.988       | 5.75          | 53.60  | 0.575       | 0.976       |

Table 1. The gene selection performances of different methods in simulation experiments.

|                | logistic | AL-lo | SSL-lo | ASSL-lo | Auto-ASSL(A) | Auto-ASSL(B) |
|----------------|----------|-------|--------|---------|--------------|--------------|
| Group A        | 0.9584   | 0.9723| 0.9709 | 0.9874  | 0.9448       | 0.9810       |
| Group B        | 0.9682   | 0.9855| 0.9796 | 0.9943  | 0.9738       | 0.9917       |

Table 2. The AUC obtained by different methods in simulation experiments.

![Figure 2. The classification accuracy of different methods in simulation experiments.](image)

![Figure 3. The ROC curves of different methods in simulation experiments.](image)
number of selected genes (NS), sensitivity and specificity are used to evaluate the gene selection performances of the methods. Supposing true positive (TP) is the number of identified disease related genes, false positive (FP) is the number of selected unrelated genes, false negative (FN) is the number of disease related genes which are missed, and true negative (TN) is the number of the unrelated genes that are abandon by different models. The sensitivity and specificity can be expressed as:

\[
sensitivity = \frac{TP}{TP + FN}
\]

| Dataset    | Number of genes | Number of samples | Number of labeled samples | Disease types         |
|------------|-----------------|-------------------|---------------------------|-----------------------|
| DLBCL      | 2648            | 77                | 26                        | diffuse large b-cell lymphoma |
| Prostate   | 2135            | 102               | 34                        | prostate cancer       |
| GSE21050   | 54613           | 310               | 103                       | soft tissue sarcomas  |
| GSE32603   | 13200           | 231               | 77                        | breast cancer         |

Table 3. Details of real datasets used in the experiments.

| Method      | DLBCL     | Prostate   | GSE21050   | GSE32603   |
|-------------|-----------|------------|------------|------------|
| logistic    | 77.94%    | 86.54%     | 79.01%     | 69.69%     |
| AL-lo       | 83.15%    | 91.53%     | 84.43%     | 73.68%     |
| SSL-lo      | 81.82%    | 88.97%     | 80.92%     | 70.57%     |
| ASSL-lo     | 87.14%    | 94.42%     | 89.34%     | 80.63%     |
| Auto-ASSL(A)| 80.67%    | 88.55%     | 78.33%     | 68.48%     |
| Auto-ASSL(B)| 85.62%    | 93.36%     | 86.37%     | 76.46%     |

Table 4. The classification accuracy obtained by different methods in the real datasets.

Figure 4. ROC curves obtained by different methods in real datasets (a) DLBCL (b) Prostate (c) GSE21050 (d) GSE32603.
The gene selection performances of different methods in simulation experiments are shown in Table 1, the results are the average of 100 runs of the program. It is easy to find the specificity obtained by single logistic regression model is highest than any other methods, it means it doesn’t select too many unrelated genes. However the lowest sensitivity shows single logistic regression model selects the least disease related genes. The AL-lo achieves a closed specificity value compared to single logistic model, but it identifies more disease related genes. The SSL-lo selects more disease related genes than single logistic model, and meanwhile many unrelated genes are also selected. Through combining the AL and SSL, the ASSL-lo identifies most disease related genes, but the problem is that it also selects more disease unrelated genes than SSL-lo. Auto-ASSL(A) selects less correct genes compared to ASSL, and the numbers of selected unrelated genes are closed. Compared to the Auto-ASSL(A), the gene selection performance obtained by Auto-ASSL(B) is obviously improved. The sensitivity obtained by Auto-ASSL(B) is only less than ASSL-lo but higher than any other methods, and the specificity is even more than the ASSL-lo. It shows that the Auto-ASSL(B) can achieve a balance between the sensitivity and specificity, and it has a strong ability to identify the disease related genes meanwhile eliminates the interference of unrelated genes.

The values of classification accuracy obtained by different methods in the unlabeled data are shown in Fig. 2. The ROC curves obtained by different methods in one run of the program are shown in Fig. 3. And the AUC values corresponding to the ROC curves are given in Table 2. The ASSL logistic model achieves the best result through combining the AL and SSL, however it needs much time and cost for manual labeling. The performance obtained by Auto-ASSL(A) is even worse than SSL logistic model, this result proves the misclassified uncertain

\[
\text{specificity} = \frac{TN}{TN + FP}
\]

Table 5. The AUC obtained by different methods in the real datasets.

| Method     | DLBCL | Prostate | GSE21050 | GSE32603 |
|------------|-------|----------|----------|----------|
| logistic   | 0.9199| 0.9569   | 0.8975   | 0.7557   |
| AL-lo      | 0.9295| 0.9749   | 0.9394   | 0.8328   |
| SSL-lo     | 0.8942| 0.9708   | 0.9232   | 0.7962   |
| ASSL-lo    | 0.9583| 0.9862   | 0.9596   | 0.9023   |
| Auto-ASSL(A) | 0.8333| 0.9646   | 0.8835   | 0.7757   |
| Auto-ASSL(B) | 0.9391| 0.9785   | 0.9432   | 0.8390   |

Table 6. The genes selected by different methods in DLBCL.

|      | logistic | AL-lo | SSL-lo | ASSL-lo | Auto-ASSL(A) | Auto-ASSL(B) |
|------|----------|-------|--------|---------|--------------|--------------|
| 1    | SELENOP  | SELENOP| SELENOP| SELENOP | SELENOP      | MDM4         |
| 2    | KIF2C    | MT2A  | PURA   | CD54    | GPR18        | SELENOP      |
| 3    | MT2A     | MIF   | MT2A   | TXNIP   | ESD          | MIF          |
| 4    | MORC3    | GLIPR1| GLIPR1 | MT2A    | GLIPR1       | MORC3        |
| 5    | TLE4     | TLE4  | TLE4   | PURA    | TLE4         | TLE4         |
| 6    | SELL     | BM11  | MIF    | TRIB2   | MYCLP1       | SELL         |
| 7    | N4BP2L1  | HFTM2 | N4BP2L1| GAPDH   | TRIM23       | N4BP2L1      |
| 8    | GLIPR1   | GAPDH | SELL   | MYCLP1 | TLE4         | GLIPR1       |
| 9    | EFNA3    | CCL21 | CCL21  | GLIPR1 | KIF2C        | CCL21        |
| 10   | MYCLP1   | SMAD6 | ESD    | MIF    | GAPDH        | MT2A         |

Table 7. The genes selected by different methods in Prostate.

|      | logistic | AL-lo | SSL-lo | ASSL-lo | Auto-ASSL(A) | Auto-ASSL(B) |
|------|----------|-------|--------|---------|--------------|--------------|
| 1    | SELENOP  | SELENOP | SELENOP | SELENOP | SELENOP      | MDM4         |
| 2    | KIF2C    | MT2A  | PURA   | CD54    | GPR18        | SELENOP      |
| 3    | MT2A     | MIF   | MT2A   | TXNIP   | ESD          | MIF          |
| 4    | MORC3    | GLIPR1| GLIPR1 | MT2A    | GLIPR1       | MORC3        |
| 5    | TLE4     | TLE4  | TLE4   | PURA    | TLE4         | TLE4         |
| 6    | SELL     | BM11  | MIF    | TRIB2   | MYCLP1       | SELL         |
| 7    | N4BP2L1  | HFTM2 | N4BP2L1| GAPDH   | TRIM23       | N4BP2L1      |
| 8    | GLIPR1   | GAPDH | SELL   | MYCLP1 | TLE4         | GLIPR1       |
| 9    | EFNA3    | CCL21 | CCL21  | GLIPR1 | KIF2C        | CCL21        |
| 10   | MYCLP1   | SMAD6 | ESD    | MIF    | GAPDH        | MT2A         |

The gene selection performances of different methods in simulation experiments are shown in Table 1, the results are the average of 100 runs of the program. It is easy to find the specificity obtained by single logistic regression model is highest than any other methods, it means it doesn’t select too many unrelated genes. However the lowest sensitivity shows single logistic regression model selects the least disease related genes. The AL-lo achieves a closed specificity value compared to single logistic model, but it identifies more disease related genes. The SSL-lo selects more disease related genes than single logistic model, and meanwhile many unrelated genes are also selected. Through combining the AL and SSL, the ASSL-lo identifies most disease related genes, but the problem is that it also selects more disease unrelated genes than SSL-lo. Auto-ASSL(A) selects less correct genes compared to ASSL, and the numbers of selected unrelated genes are closed. Compared to the Auto-ASSL(A), the gene selection performance obtained by Auto-ASSL(B) is obviously improved. The sensitivity obtained by Auto-ASSL(B) is only less than ASSL-lo but higher than any other methods, and the specificity is even more than the ASSL-lo. It shows that the Auto-ASSL(B) can achieve a balance between the sensitivity and specificity, and it has a strong ability to identify the disease related genes meanwhile eliminates the interference of unrelated genes.
samples have significant bad effect on the classification performance and our update mechanism is very necessary for Auto-ASSL. The results show our method is advanced because it achieves higher accuracy than AL-lo or SSL-lo and only less than ASSL-lo, and meanwhile it doesn’t need any manual labeling. Hence the new logistic regression model combing SSL and AL can be seen as a very efficient method because it implements the following functions:

1. It works without any manual intervention. This saves much cost and the results can be quickly obtained.
2. It can achieve accuracy above 90% in disease classification. The experiments show our method can achieve a better accuracy than the AL and SSL logistic regression models.

Table 8. The genes selected by different methods in GSE21050.

| logistic | AL-lo | SSL-lo | ASSL-lo | Auto-ASSL(A) | Auto-ASSL(B) |
|----------|-------|--------|---------|--------------|--------------|
| 1 C1serf41 | SNAPC1 | SNAPC1 | FAD61 | MTHFD2 | MTHFD2 |
| 2 SNAPC1 | SNORD35B | C8orf82 | SNORD35B | ADD3 | SNORD35B |
| 3 C8orf82 | MTHFD2 | MTHFD2 | IFT43 | SNAPC1 | SNAPC1 |
| 4 MTHFD2 | NFATC2IP | SLCA1A | C8orf82 | SNORD35B | ADD3 |
| 5 LPAR1 | C8orf82 | PML | CDC24E3 | FHL2 | C8orf82 |
| 6 AKT2 | NUP155 | PLD1 | MTHFD2 | PCDH18 | XPO6 |
| 7 XPO6 | XPO6 | WDHD1 | DCN | NEATC2IP | ATP6V1D |
| 8 SLC1A1 | IFT43 | AKT2 | SNAPC1 | YEATS2 | IFT43 |
| 9 PLD1 | PCDH18 | RPL13A | XPO6 | LIMK2 | NUP155 |
| 10 SNORD35B | WDHD1 | NFATC2IP | ADD3 | SMAD4 | ENO2 |

Table 9. The genes selected by different methods in GSE32603.

| logistic | AL-lo | SSL-lo | ASSL-lo | Auto-ASSL(A) | Auto-ASSL(B) |
|----------|-------|--------|---------|--------------|--------------|
| 1 ROR2 | GRB2 | LOC642236 | ROR2 | ROR2 | EMB |
| 2 LOC642236 | MS4A1 | ROR2 | EMB | EMB | ROR2 |
| 3 GRB2 | EM8 | GRB2 | ZSCAN9 | GRB2 | GRB2 |
| 4 EM8 | ROR2 | EMB | CDKN1B | TMEM242 | TMEM242 |
| 5 MAST1 | UBE2W | UPCA | HPSE |
| 6 C2orf70 | EPHB1 | CORD3 | TPD52L2 |
| 7 TAF8 | SUPT20H |
| 8 MTSS1 | ARL2BP |
| 9 PRDM4 | STK3 |

Figure 5. The number of genes selected by different methods in real datasets.
Real data experiments. In real data experiments six methods are applied on four real gene expression datasets: Diffuse large B-cell lymphoma (DLBCL) dataset, Prostate cancer dataset, GSE21050 and GSE32603. In these four datasets about 2/3 samples are treated as the unlabeled samples for evaluating the classification accuracy of unlabeled samples. The labeled samples and unlabeled samples are randomly selected in every runs of the program. More details of the datasets used in the experiments are shown in Table 3.

The values of classification accuracy obtained by different methods in real datasets are shown in Table 4. The ROC curves obtained by different methods in one run of the program in different datasets are shown in Fig. 4, and the corresponding AUC are shown in Table 5. The SSL-lo performs better than single logistic and Auto-ASSL(A), but worse than the other three methods. It is obviously that the accuracy of ASSL logistic model is highest. The Auto-ASSL(A) does not perform well because the misclassified samples affect the accuracy. The classification accuracy obtained by Auto-ASSL(B) is better than any other methods except ASSL which proves that the update pseudo-labeled samples mechanism is a very important improvement for the model.

The numbers of genes selected by different methods in real dataset are shown in Fig. 5. It is obvious that the single logistic method selects least genes. The numbers of selected genes obtained by ASSL and Auto-ASSL(A) are far more than other methods. Our method selects more genes than AL-lo and SSL-lo, but less than ASSL-lo.

In order to further assess the correctness of the selected genes by different methods, the top-10 ranked genes selected by different methods in real datasets are listed in Tables 6–9. Table 9 is partly blank because the methods didn’t select so many genes. The genes in italic in the tables such as SELENOP, HPN, MTHFD2 and ROR2 are the ones which are selected by all the methods in the same datasets. The SELENOP in DLBCL can be seen as an extracellular antioxidant, and it may be potential non-invasive diagnostic markers for cancer. Some researches show that selenium could be seen as an anticancer therapy by affecting SELENOP extracellular antioxidant, and it may be potential non-invasive diagnostic markers for cancer. The research has proved that expression of the encoded protein of HPN is related to the growth and progression of cancers, particularly prostate cancer. It may be associated with susceptibility to prostate cancer. The MTHFD2 in GSE32603 is seen as a prognostic factor and a potential therapeutic target for future cancer treatments. The ROR2 in GSE32603 is reported that it can significantly reduce cell proliferation and induced apoptosis.

On the other hand, our method also identified some special genes which other methods did not select.

These genes are shown in bold in the Tables 6–9. The MDM4 in DLBCL plays a very important role in the proliferation of the cancer cells, and it is crucial for the establishment and progression of tumors. JUNB plays a specific role in cancer cell proliferation, survival and drug resistance. Single nucleotide polymorphism of TIPARP in Prostate has been proved to be related with cancer. The TPD52L2 in GSE32603 encodes a member of the tumor protein D52-like family, and contributes to proliferation of cancer cells. These genes mentioned in the literatures demonstrate that our new logistic regression model has a strong ability in gene selection.

Conclusion
In this paper we have designed a novel method which does not require significant engineering overhead to use and meanwhile achieve satisfying results by utilizing the unlabeled gene expression samples in disease classification. The novel logistic regression model is designed based on the complementarity of semi-supervised learning and active learning. In addition to that, an update pseudo-labeled samples mechanism is embedded in this method to reduce the false pseudo-labeled samples. In conclusion, our method can achieve more accuracy results compared widely used SSL and AL logistic models, and it also has a good performance in identifying the disease related genes. In addition to that, this model can work without any manual labeling for saving much time and cost. We believe it will be an efficient tool to make contributions for disease classification and gene selection because of its high reliability and stability against noise and outliers.

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**Author Contributions**

H.C. proposed the new logistic model and designed the code. Y.L. wrote the manuscript, S.W. and H.W.S. designed the algorithm and provided the real data. All authors reviewed the manuscript.

**Additional Information**

**Competing Interests:** The authors declare no competing interests.

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