Dark gauge bosons: LHC signatures of non-abelian kinetic mixing

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ABSTRACT

We consider non-abelian kinetic mixing between the Standard Model SU(2)L and a dark sector U(1)′ gauge group associated with the presence of a scalar SU(2)L triplet. The magnitude of the resulting dark photon coupling ϵ is determined by the ratio of the triplet vacuum expectation value, constrained to by \( \lesssim 4 \) GeV by electroweak precision tests, to the scale \( \Lambda \) of the effective theory. The corresponding effective operator Wilson coefficient can be \( \mathcal{O}(1) \) while accommodating null results for dark photon searches, allowing for a distinctive LHC dark photon phenomenology. After outlining the possible LHC signatures, we illustrate by recasting current ATLAS dark photon results into the non-abelian mixing context.

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1. Introduction

The search for weakly coupled light vector bosons has been a subject of considerable interest in recent years. Searches have been carried out in a number of different contexts, including low energy colliders, meson decays, beam dump experiments, and high-energy colliders (see, e.g., Refs. [1,2] and references therein). Theoretical studies typically assume that interactions of the “dark photon” with the visible sector are mediated by abelian kinetic mixing between the Standard Model (SM) hypercharge and the dark U(1)′ gauge groups [3–5]. For the “dark Z”, mixing with the SM Z-boson may also occur via the mass terms in the Lagrangian [6,7]. For both abelian and mass-mixing, the effects arise at the level of renormalizable operators. The resulting coupling of the dark vector bosons to the SM are then parameterized by a dimensionless parameter \( \epsilon \) that is constrained by experiment to be \( \lesssim 10^{-3} \) or smaller when for dark boson masses below \( \sim 10 \) GeV. The small scale of \( \epsilon \) has no obvious origin in this context, so one must resort to models to explain why it is not \( \mathcal{O}(1) \).

In this study, we observe that non-abelian mixing between the U(1)′ and the SM SU(2)L gauge groups, encoded in non-renormalizable operators, can provide a simple explanation without assuming tiny operator coefficients in the effective theory. Doing so requires augmenting the SM field content with additional bosons gauge bosons transforming non-trivially under SU(2)L. For concreteness, we consider the scalar triplet \( \Sigma \sim (1, 3, 0, 0) \) and focus on the dimension-five operator

\[
\mathcal{O}_{WX}^{(5)} = -\frac{\beta}{\Lambda} \text{Tr}(W_{\mu\nu} \Sigma) X^{\mu\nu}
\]

(1.1)

where \( X^{\mu\nu} \) and \( W^{\mu\nu} \) are the U(1)′ and SU(2)L field strength tensors, respectively; \( \Sigma = \Sigma^T \) with \( \Sigma^T \) being the SU(2)L generators; and \( \Lambda \) is the mass scale associated with fields that have been integrated out in generating the operator. A non-zero vacuum expectation value \( \langle \Sigma \rangle \neq 0 \) will lead to mixing between the U(1)′ boson \( X_\mu \) and the neutral SU(2)L gauge boson \( W^3_\mu \). The mixing parameter is then given by

\[
\epsilon = \beta \sin \theta_W \left( \frac{v \Sigma}{\Lambda} \right).
\]

(1.2)

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where $\theta_W$ is the weak mixing angle. For non-vanishing mixing parameter, $X_{\mu}$ inherits all couplings of the photon to SM fermions but rescaled by the universal factor $\epsilon$, whose magnitude is controlled by the scale ratio $v_{\Sigma}/\Lambda$. Importantly, constraints from electroweak precision tests constrain the triplet vev to be relatively small: $v_\Sigma \lesssim 4$ GeV. Thus, $\epsilon$ will satisfy the experimental bounds for $\Lambda$ larger than about one TeV for $\beta/\Lambda \sim O(1)$.

The idea of non-abelian kinetic mixing is not original to us. The authors of Ref. [8] considered $U(1)' \times SU(2)'$, with the latter factor being a dark SU(2) gauge group [9]. Dark SU(2) gauge invariance requires introduction of an additional scalar triplet $\Sigma_2 \sim (1,1,0,3)$, allowing for a dimension five mixing operator analogous to that of Eq. (1.1). In contrast to the present case, however, the dark triplet vev can have any magnitude, and for large values, a small $\epsilon$ requires a commensurately small operator coefficient. In a follow-up work [10] applications for astrophysical and other constraints are studied in this scenario. In Ref. [11] this non-abelian kinetic mixing is used to explain the X-ray line at 3.55 keV.

More recently, the authors of Ref. [12] considered $SU(2)_{L'} \times U(1)'$ kinetic mixing via the dimension six operator

$$\frac{C}{\Lambda^2} H^T \Theta H W_{\mu \nu} X^{\mu \nu} \tag{1.3}$$

where $H$ is the SM Higgs doublet, leading to $\epsilon \sim C(\nu/\Lambda)^2$. Assuming this operator arises at one-loop, one has $\Lambda \sim 4\pi m_{\psi}$, where $m_{\psi}$ is the mass of the mediator $\psi$ in the loop. For $\Lambda \gtrsim 10$ TeV (or $m_{\psi} \gtrsim 1$ TeV), one may satisfy the experimental constraints on $\epsilon$ for $C \sim O(1)$. The authors of this work consider an explicit model with a scalar mediator $\psi \sim (1,3,0,q_3)$ and a dark Higgs $H_D \sim (1,1,0,q_D)$ that is responsible for generating the dark photon mass. A detailed analysis of the collider signatures associated with the dark bosons is given.

In what follows, we concentrate on the collider signatures associated with the dimension five operator (1.1) rather than on construction of an explicit dark sector mediator model. In particular, we note that final states containing one or more $X$ bosons may be produced through two distinct mechanisms, each of which involves $O_{WX}^{(5)}$ directly: (1) Drell–Yan pair production of $\Sigma$ states, $pp \rightarrow V \rightarrow \Sigma X$, followed by the $O_{WX}^{(5)}$-induced decay $\Sigma \rightarrow VX$, resulting in a $XXV$ topology; (2) direct production via $O_{WX}^{(5)}$, $pp \rightarrow V^* \rightarrow \Sigma X$, followed by the decay $\Sigma \rightarrow VX$, generating a final state of the topology $XXV$. For sufficiently large $\beta/\Lambda$ the direct production mechanism (2) may dominate. In this case, $\nu_\Sigma$ must be sufficiently small to ensure the experimental constraints on $\epsilon$ are satisfied. Conversely, for smaller $\beta/\Lambda$ (larger $\nu_\Sigma$ for a given $\epsilon$), production will occur primarily through the Drell–Yan process.

For similar reasons, the $\Sigma$-decay branching ratios will also carry a dependence on $\beta/\Lambda$ (and, thus, on $\nu_\Sigma$ for fixed $\epsilon$). In what follows, we delineate several general parameter space regimes associated with this interplay of parameters.

For concrete illustration, we then consider the present LHC sensitivity for the regions of parameter space where the direct production mechanism dominates and where the $\Sigma \rightarrow VX$ branching ratio is close to unity. For this parameter space region and for $m_X > 2m_{\mu}$, one expects displaced vertices associated with $X \rightarrow \mu^+\mu^-$ decays, where the dimuon pair appears as a lepton jet. The ATLAS collaboration has performed a search for events of this type that involve two or four lepton jets [13]. We carry out a simple re-cast of the corresponding ATLAS bound on long-lived dark bosons for our scenario, noting that the ATLAS search is inclusive and accommodates additional, unobserved, final state SM gauge bosons. For dark boson mass $m_X$ in the range 0.2 GeV $\leq m_X \leq 2$ GeV we find that the present ATLAS exclusion can extend to $\Lambda/\beta \sim$ several hundred GeV, depending on the value of $\nu_\Sigma$. As we discuss in Section 4, the present reach may lie on the border of the region of validity of the effective theory. Consequently, one should consider our results as indicative of the LHC 8 TeV sensitivity to the parameters of this scenario rather than as quantitatively definitive. We, thus, also discuss the possibilities for future LHC tests of this scenario that would probe higher mass scales, including searches that would identify the SM final state gauge bosons.

Our discussion of this scenario and collider analysis is organized as follows. In Section 2 we review the setup of the triplet-assisted non-abelian kinetic mixing. In Section 3 we outline distinctive LHC signatures for our scenario and in Section 4 we present the re-cast of ATLAS bounds on dark photons for the non-abelian kinetic mixing. Finally, we conclude in Section 5.

2. The model

We add to SM Lagrangian dimension four operators involving dark photon and the real triplet fields, as well as dimension five effective operators:

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \Delta \mathcal{L}^{d=4} + \Delta \mathcal{L}^{d=5} + \ldots \tag{2.1}$$

The dimension four and five operators we take to be of the form:

$$\Delta \mathcal{L}^{d=4} = \frac{-1}{4} X_{\mu \nu} X^{\mu \nu} + \frac{\epsilon_0}{2 \epsilon_W} B_{\mu \nu} X^{\mu \nu} + \text{Tr} \left( D_{\mu} \Sigma \right)^T D_{\mu} \Sigma - V(\Sigma, H) + \Delta \mathcal{L}^{d=4}$$

$$\Delta \mathcal{L}^{d=5} = -\frac{1}{\Lambda} \text{Tr} \left( W_{\mu \nu} \Sigma \right) \left( a B_{\mu \nu} + \beta X^{\mu \nu} \right) \equiv O_{WB}^{(5)} + O_{WX}^{(5)}. \tag{2.2}$$

Here, $\Delta \mathcal{L}^{d=4}$ contains the usual abelian $(X^B)$ kinetic mixing term and $\epsilon_W$ is the cosine of the weak mixing angle. The terms breaking the dark $U(1)'$ gauge group are not explicitly presented and are part of $\Delta \mathcal{L}^{d=4}$. The real triplet field $\Sigma$ and the scalar triplet-doublet potential are given by [14]:

$$\Sigma = \frac{1}{2} \begin{pmatrix} \Sigma^0 & \sqrt{2} \Sigma^+ \\ \sqrt{2} \Sigma^- & -\Sigma^0 \end{pmatrix}, \tag{2.3}$$

$$D_{\mu} \Sigma = \partial_{\mu} \Sigma + ig \sum_{a=1}^{3} W_{\mu}^a T^a, \Sigma \tag{2.4}$$

$$V(H, \Sigma) = -\mu^2 H^\dagger H + \lambda_0 \left( \text{Tr} H^\dagger H \right)^2 - \mu_2^2 G + b_4 G^2 + a_1 H^\dagger \Sigma H + a_2 H^\dagger HG, \tag{2.5}$$

where $G = \text{Tr} \Sigma^\dagger \Sigma = \frac{1}{2} \Sigma^2 + \Sigma^+ \Sigma^-$. In the notation of Ref. [14], $G = F/2$.

Given a UV complete theory one may integrate out heavy states that have both SM and dark charges, as illustrated in Fig. 1. We leave the model-dependent details of the full theory unspecified, focusing instead on $O_{WX}^{(5)}$ and the corresponding collider phenomenology. In addition it is possible that similar graphs as in Fig. 1 generate the effective dimension five operator $O_{WB}^{(5)}$. After
electroweak symmetry breaking (EWSB), this operator will contribute to the $S$ parameter:

$$
\alpha_{\text{em}} S = 4c_W s_W \frac{\alpha v \Sigma}{\Lambda}.
$$

(2.5)

This sets a 90% CL bound $\alpha v \Sigma / \Lambda \lesssim 0.0008$. We will henceforth set $\alpha = 0$ and concentrate on the phenomenology associated with $\mathcal{O}^{(5)}_{WX}$.

Before proceeding, we comment here that kinetic mixing of gauge bosons can also be realized for non-abelian groups. For example, for a $SU(N) \times SU(M)$ gauge theory with gauge fields $W$ and $Y$, one can introduce a scalar field $\Delta^{ab}$ transforming as the adjoint representation under both the $SU(N)$ and $SU(M)$ groups, with indices “a” and “b” corresponding to $SU(N)$ and $SU(M)$, respectively. In analogy with $\mathcal{O}^{(5)}_{WX}$, one can construct the $d = 5$ operator $W^{a/1} v^{b/1} \Delta^{ab}$. A non-vanishing vev for $\Delta^{ab}$ will lead to kinetic mixing between $W$ and $Y$. One may also construct renormalizable models that generate this operator at the one-loop level. We defer a detailed consideration of this possibility to a future study.

3. Collider phenomenology

In the presence of $\mathcal{O}^{(5)}_{WX}$, the collider phenomenology associated with the real triplet can differ substantially from what has been considered previously in Ref. [14]. To illustrate the key features, we will make the following assumptions:

(a) The potential parameters are chosen so as to render the doublet-triplet mixing angle $\theta$ proportional to $\alpha v \Sigma$ to be small, but non-vanishing. In this case the neutral scalar sector will consist of two states, $H_{1,2}$, with $H_1$ being primarily the SM Higgs boson and $H_2$ being primarily $\Sigma^0$. In the charged scalar sector, doublet-triplet mixing implies that the physical charged triplet states $H^\pm$ are not pure triplet states, but rather mixtures of $\Sigma^\pm$ and the charged components of the doublet, with the other combination providing the longitudinal components of the massive weak gauge bosons. Note that in the absence of doublet-triplet mixing, $SU(2)_L \times U(1)_Y$ gauge invariance precludes $\Sigma^0$ from coupling to the SM fermions. The presence of a non-vanishing mixing angle then introduces a coupling of $H^\pm, H_2$ to the SM fermions through the SM Yukawa interactions.

(b) For $v \Sigma = 0$, the triplet states have a common mass, give by $m_\Sigma^2 = -\mu_\Sigma^2 + \alpha v^2/2$. Electroweak loops raise the mass of the charged components with respect to that of the neutral component by $\sim 166$ MeV, allowing for the decay $H^+ \rightarrow H_2 \pi^+$. Our choice of the potential parameters will not substantially alter this splitting even for $v \Sigma \neq 0$.

With these comments in mind, we now consider the production and decays of the triplet-like scalars.

3.1. Production

The LHC production and decay mechanisms of interest are shown in Fig. 2. Graphs (a) and (b) indicate Drell–Yan pair production, $pp \rightarrow V^* \rightarrow \phi \phi$, where $\phi$ denotes any of the physical scalars, with the subsequent decays $\phi \rightarrow XV$, leading to the topology $XXV$. As discussed above, the $\phi$ states will be predominantly triplet-like. Graphs (c) and (d) show the $\mathcal{O}^{(5)}_{WX}$-mediated production $pp \rightarrow V^* \rightarrow \phi X$, with a subsequent decay $\phi \rightarrow XV$, leading to the topology $XXV$. (Feynman rules for the vertices in Fig. 2 are listed in the Appendix A.)

In Fig. 3 we show the LHC production cross sections for different channels at $\sqrt{s} = 8$ TeV. The left panel corresponds to $m_\phi = 130$ GeV and the right one corresponds to $m_\phi = 300$ GeV. For both masses we observe that for $\beta / \Lambda \lesssim 1 / \text{TeV}$ the Drell–Yan pair production dominates, while for $\beta / \Lambda \gtrsim 1 / \text{TeV}$ $\mathcal{O}^{(5)}_{WX}$-mediated production is the dominant mechanism. For $\sqrt{s} = 14$ TeV the corresponding transition between Drell–Yan and $\mathcal{O}^{(5)}_{WX}$-mediated production occurs for approximately the same value of $\beta / \Lambda$.

3.2. Triplet-like scalar decay branching ratios

The triplet-like scalars $H^\pm$ and $H_2$ will decay to $W^\pm X$ and $Z/\gamma X$ respectively as well as to other final states as considered

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3 For generic choices of scalar potential parameters, the magnitude of the neutral doublet-triplet mixing angle falls well below the upper bound implied by Higgs boson signal strengths [15]. See Ref. [14] for a detailed analysis of the dependence of the mixing angle on the potential parameters.
in Ref. [14]. For illustrative purposes we show the decay width for $H^{\pm} \to W^{\pm} X$, which is sufficient for the analysis that we consider below. The tree level $H^\pm \to W^\pm X$ decay rate is given by

$$
\Gamma(H^{\pm} \to W^{\pm} X) = \frac{1}{16\pi M_{H^\pm}} \left[ \frac{2(m_W^2 + M_{H^\pm}^2)}{M_{H^\pm}^2} + \frac{(m_W^2 - M_{W^\pm}^2)^2}{M_{H^\pm}^2} + \frac{1}{2} \left( \frac{M_{H^\pm}^2 - m_X^2 - M_{W^\pm}^2}{M_{H^\pm}^2} \right)^2 + \frac{m_X^2 M_{W^\pm}^2}{M_{H^\pm}^2} \right] \times \frac{B_{\tau}^2}{\Lambda^2},
$$

where $c_\Sigma$ is the mixing angle associated with diagonalizing the charged scalar sector. Combined with the other $H^+$ decay channels [14] we compute the branching ratios shown in Fig. 4. The left and right panels correspond to $m_{H^+} = 130$ GeV and $m_{H^+} = 300$ GeV, respectively. The top panels correspond to $v_\Sigma = 1$ GeV and the bottom ones to $v_\Sigma = 1$ MeV.

From the plots in Fig. 4 we see that for $v_\Sigma = 1$ GeV, a value near the maximum allowed by electroweak precision tests, the branching ratio for $H^+ \to W^+ X$ is essentially 100% when $\epsilon \gtrsim 10^{-4}$. For the smaller value of $v_\Sigma = 1$ MeV, the branching ratio is essentially 100% for all values of $\epsilon$. This translates into the range $\beta/\Lambda \gtrsim 0.1/\text{TeV}$ for the branching ratio to be essentially 100% independent of the value of the vev. For lower values of $\beta/\Lambda$ any branching ratio from zero to one is possible, and the precise value depends strongly on the value $v_\Sigma$. 

Fig. 3. Production cross sections for $pp \to V \to \phi \phi$ and $pp \to V \to X \phi$ for associated triplet-like states $\phi = H^+, H_2$ and a dark photon $X$ with mass $m_X = 0.4$ GeV. For the final states containing a single charged scalar and one neutral boson, we have summed the cross sections for both charges (e.g. $\sigma(\phi^+ H_2) + \sigma(\phi^- H_2)$). The left and right panels correspond to $m_\phi = 130$ GeV and $m_\phi = 300$ GeV, respectively. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Fig. 4. Branching ratios for $H^+$ decays as a function of $\beta/\Lambda$ (bottom horizontal axis) and $\epsilon$ (upper horizontal axis) for $m_X = 0.4$ GeV. The top (bottom) row corresponds to $v_\Sigma = 1$ GeV ($v_\Sigma = 10^{-3}$ GeV), while the left (right) column corresponds to $m_{H^+} = 130$ GeV ($m_{H^+} = 300$ GeV). The solid black line indicates the branching ratio for $H^+ \to W^+ X$. Branching ratios for other final states are as indicated by the legend insert. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
3.3. Various regimes for collider phenomenology

From the foregoing discussion of production and decays, the LHC signatures and detection strategies will vary according to the value of $\beta/\Lambda$. We delineate three regimes leading to distinctive phenomenology for 8 TeV pp center of mass energy:

(1) $\beta/\Lambda \sim 1/\text{TeV}$. In this regime we see that Drell–Yan pair production $p \to \phi \phi$ dominates. In addition the branching ratio for $\phi \to X \nu \nu$ decay is close to hundred percent.

(2) $\beta/\Lambda \lesssim 0.1/\text{TeV}$. In this regime Drell–Yan pair production remains the dominant mechanism. However, BR($\phi \to X \nu \nu$) can range from zero to one, depending on value of $v_\Sigma$.

(3) $\beta/\Lambda \gtrsim 1/\text{TeV}$. In this regime the $O_{WX}^{(5)}$-mediated process $pp \to X \phi$ is dominant and BR($\phi \to X \nu \nu$) is close to one. In this case, the possible final states are indicated in Fig. 2(c, d).

(Recall that for $\sqrt{s} = 14$ TeV, the transition between $O_{WX}^{(5)}$-mediated production and Drell–Yan pair production also occurs for $\beta/\Lambda \sim 1/\text{TeV}$.) While all three possibilities above are worth exploration in future, for illustrative purposes we focus here on the third regime.

4. ATLAS recast

Considering the above regime (3), we recast the ATLAS dark photon search results [13] into constraints on our scenario. The analysis of Ref. [13] assumes the presence of a SM Higgs boson decaying to two new states that radiate two (or four) dark photons, leading to displaced vertices and lepton jets. This is to be compared to our production scenario mediated by an off-shell vector boson $V^*$, leading to a final state containing two $X$ bosons and an on-shell $V$. Note, that the ATLAS study [13] only applied cuts to isolate events with lepton jets and displaced vertices. No reconstruction of the Higgs boson invariant mass was performed, nor were cuts on the missing energy applied. Thus, although the ATLAS study was carried out assuming different underlying $X$-boson production dynamics, the analysis is sufficiently inclusive to accommodate the scenario considered here as well. Looking to the future, we note that one could likely improve the LHC sensitivity to $O_{WX}^{(5)}$ by including additional criteria needed to identify the final state $V$.

We then translate the ATLAS bounds on $\epsilon - m_X$ parameter space [13] to the parameter space relevant to our scenario. Consequently, we are able to exclude the $(\epsilon, m_X)$ plane in the $(\epsilon, m_X)$ plane. The left panel gives the exclusion region in the $(\epsilon, m_X)$ plane for $m_X = 0.4$ GeV (red region) and $m_X = 1.5$ GeV (yellow region). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

![ATLAS](image)

**Fig. 5.** Constrains on triplet-assisted non-abelian kinetic mixing, recast from the ATLAS search reported Ref. [13]. The left panel gives the exclusion in the $(\epsilon, m_X)$ plane for $m_X = 0.4$ GeV (red region) and $m_X = 1.5$ GeV (yellow region). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

4 This bound is obtained by excluding from the analysis $\gamma Z\gamma Z$ events, which correspond to both dark photons decaying to jets. This leads to a stronger bound due to corresponding backgrounds.
possibilities: (a) loops involving new vector-like fermions; (b) loops involving new scalars; (c) non-perturbative dynamics. We comment on the first two possibilities. Considering new vector-like fermions $F$ with mass $M_F$, naive dimensional analysis suggests that $\Lambda/\beta \sim 20\pi^2 M_F^2/\gamma$, where $\gamma$ is the $F F \Sigma$ coupling and where we take the gauge couplings to be $O(1)$. Since $F$ carries SU(2) charge, it would likely have been observed if sufficiently light. For example, the non-observation of pairs of new charged particles (e.g., vector-like leptons) at LHC [16], may imply a lower bound of 200 GeV $\lesssim M_F$ in some cases, implying $\Lambda/\beta \gtrsim 3.2$ TeV for $\gamma \sim O(1)$. Significantly larger integrated luminosity and/or a search that exploits final state gauge boson reconstruction would be needed to reach this level of sensitivity. For new electroweak scalars $S$ with mass $M_S$, one has $\Lambda/\beta \sim 16\pi^2 M_S^2 F_S/\gamma S$, where $\gamma_S$ is the $S S \Sigma$ coupling with dimensions of mass, and $F_S$ will depend in part on the SU(2) representation of $S$. Assuming $M_S \gtrsim 100$ GeV in order to evade LEP II limits and taking $\gamma_S \sim 1$ (and, $F_S = 0$) to be of order $O(1)$, it also gives $\Lambda/\beta \sim 1.6$ TeV. However, nothing precludes $\gamma_S$ from being a few times larger than $M_S$, so it is not unreasonable to anticipate $\Lambda/\beta$ being to the upper end of the exclusion region in Fig. 5.

It is possible for the charged triplet state $H^+ \to t$ to decay to a pair of mediators at tree-level. In order for this decay to occur, the mediator mass must be less than half $m_{H^+}$. For the limits shown in Fig. 5 and discussed above, we have taken $m_{H^+} = m_{H^0} = 130$ GeV. In this case, no tree-level decay to mediators with masses satisfying present collider bounds is possible. The other case is $m_{H^+} = 300$ GeV which was used in some of our BR plots in Fig. 4. But we did not use it in Fig. 5 in deriving our limits on $\Lambda/\beta$. Therefore, our assumption of 100% branching of $H^+ \to W^+ X$ is consistent.

Finally, it is worth noting that for internal particle masses near 100 GeV, one may be near the border of the region of validity of a pure effective theory treatment of the collider phenomenology. In principle, invoking an explicit model for generation of the operator coefficient and/or inclusion of a form factor would likely provide a more quantitatively realistic assessment. Similar considerations apply to the application of the Higgs effective theory in studies of Higgs boson observables (see, e.g., Ref. [17] for a discussion in the context of SM di-Higgs production in association with an additional, high-$p_T$ jet). In the present instance, the ATLAS lepton jet reconstruction efficiency peaks in the vicinity of $p_T > 40$ GeV, while the masses of the intermediate $H^\pm H^0$ and final state $W$-boson are not so large. Thus, we would expect at most a modest degradation of the signal strength in a more realistic, model-dependent analysis. Nonetheless, we consider our statements about the present LHC reach as indicative of the 8 TeV sensitivity rather than as quantitatively definitive.

5. Outlook

Mixing between the dark $U(1)'$ and SU(2)$_L$ gauge groups, mediated by the operator $O_{U(1)'}^{\S}$, leads to a small mixing parameter $\epsilon$, whose magnitude is set by the scale ratio $v_{S}/A$ with an $O(1)$ Wilson coefficient, $\beta$. The resulting collider phenomenology is quite distinctive, as $O_{U(1)'}^{\S}$ may dominate the production of final states containing $X$ bosons when $\Lambda/\beta \lesssim 1$ TeV at both $\sqrt{s} = 8$ TeV and $\sqrt{s} = 14$ TeV. Current ATLAS bounds, based on an inclusive search for pairs of lepton jets associated with displaced vertices, exclude $\Lambda/\beta$ up to about 600 GeV, depending on the value of $m_X$ and the triplet $v_{S}$. Looking to the future, the collection of additional data during Run II will extend the reach of the inclusive search.

In the advent of a discovery, inclusion of additional search criteria associated with the final state vector boson($s$) would allow one to distinguish this scenario from those associated with abelian kinetic mixing. An analysis of this possibility, along with the LHC sensitivity to other regions of the $(m_X, \epsilon)$ plane, will appear in future work.

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Appendix A. Feynman rules relevant for collider signatures

Feynman rules of interactions between the dark bosons, leptons, gauge bosons, charged and neutral Higgs bosons are listed in the table below:

| Interaction | Feynman rule |
|-------------|--------------|
| $X^{+}X^{-}$ | $i e (\epsilon_0 - \frac{\gamma_3 \gamma_5}{\gamma})$ |
| $W^+H^\mp X$ | $\frac{i e}{\Lambda} (g^{\nu \mu} p^\nu - p^\nu p^\mu) \epsilon_+^{\pm}$ |
| $Z H X$ | $\frac{i e}{\Lambda} (g^{\nu \mu} p^\nu - p^\nu p^\mu) c_W$ |
| $A H X$ | $\frac{i e}{\Lambda} (g^{\nu \mu} p^\nu - p^\nu p^\mu) s_W$ |
| $W_{\mu}^+(p_1)W_{\nu}^-(p_2)H^+ X_a(p_3)$ | $\frac{i e}{\Lambda} (p_{\nu} g_{\mu a} - p_{\mu} g_{\nu a}) \epsilon_0$ |
| $W_{\mu}^+(p_1)Z_{\nu}^+(p_2)H^0 X_a(p_3)$ | $\frac{i e}{\Lambda} (p_{\nu} g_{\mu a} - p_{\mu} g_{\nu a}) c_W$ |
| $W_{\mu}^+(p_1)A_{\nu}^+(p_2)H^\mp X_a(p_3)$ | $\frac{i e}{\Lambda} (p_{\nu} g_{\mu a} - p_{\mu} g_{\nu a}) s_W$ |

Feynman rules entering in the vertices of the graphs in Fig. 2. Where $\epsilon_+ \equiv \cos \theta_+ \gamma$ and $c_0 \equiv \cos \theta_0$ are as defined in Ref. [14].

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