Expected Performance of Tracking in CMS at the HL-LHC

Erica Brondolin\(^1\,^a\) on behalf of the CMS Collaboration

\(^1\) Institut für Hochenergiephysik der ÖAW (AT), Vienna, Austria

Abstract. During the Long Shutdown 3, scheduled from 2024 to mid 2026, CERN is planning an upgrade program in preparation of the High-Luminosity LHC (HL-LHC), which will bring the luminosity up to \(5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}\), almost five times the one envisaged for 2017. As a consequence, up to 200 inelastic collisions on average will be superimposed on the event of interest. In this high-occupancy environment, reconstructing charged particle momenta with high precision is one of the biggest challenges. In order to face this new scenario, called Phase 2, the Compact Muon Solenoid (CMS) experiment will build a completely new silicon tracking detector. New approaches to track finding will have to be implemented to exploit the capabilities of the new tracker in addition to the algorithms already in use. The expected performance of CMS tracking at the HL-LHC is presented in this contribution.

1 Introduction

Starting in 2026, LHC will achieve a luminosity of \(5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}\) with a bunch spacing of 25 ns. This LHC upgrade, called High-Luminosity LHC (HL-LHC), is accompanied by an upgrade program of the CMS experiment, called Phase 2, to maintain the excellent performance of the detector. In the specific case of tracking, the CMS tracker will be traversed by about 6000 charged particles with transverse momentum above 300 MeV at every cross beam, produced by about 200 collisions on average, that should be reconstructed. In order to face this challenge, CMS will install a new silicon-based tracker, which must satisfy the physics performance requirements under HL-LHC conditions.

2 The CMS tracking system in Phase 2

The present strip tracker was designed to operate efficiently up to an integrated luminosity of 500 fb\(^{-1}\) and an average pile-up of 30 to 50 collisions per bunch crossing. The effect of the radiation damage and the resulting performance degradation is extensively described in Ref. [1]. The rise of the LHC luminosity will increase the average pile-up per bunch crossing to 140–200, and the integrated luminosity at the end of the HL-LHC era is estimated to be 3000 fb\(^{-1}\). These completely new conditions will require a substantial upgrade of the CMS tracking system, which has to fulfill the following requirements:

\(^a\) e-mail: erica.brondolin@cern.ch

© The Authors, published by EDP Sciences. This is an open access article distributed under the terms of the Creative Commons Attribution License 4.0 (http://creativecommons.org/licenses/by/4.0/).
• **High radiation tolerance**: The new tracker must be able to operate efficiently for the entire HL-LHC period up to an integrated luminosity of 3000 fb$^{-1}$. While no maintenance interventions are foreseen for the Outer Tracker, the pixel modules of the Inner Tracker remain accessible and can be replaced.

• **Increased granularity**: This requirement is needed in order to avoid cluster merging and to maintain a good track separation in the Inner Tracker, and to limit the combinatorics in both the seeding and the track finding phase.

• **Contribution to the Level-1 trigger**: In Phase 2 the trigger system is expected to maintain an output rate of 100 kHz despite the tenfold luminosity. This appears to be possible only with the addition of tracking information to the CMS Level-1 trigger system.

• **Extended tracking acceptance**: As the CMS physics program will benefit from a larger acceptance region, the new tracker has been designed to cover the entire $\eta$ region up to $|\eta| = 4$.

• **Reduced material**: The degradation of the tracking performance and the overall physics performance depends strongly on the amount of material in the tracking volume, therefore a lighter tracker option has been chosen. At $\eta = 0$ and in the most forward region, i.e. $3.0 < |\eta| < 4.0$, the total amount of material inside the tracking volume is estimated as 30% of a radiation length. In the Outer Tracker region, it rises up to 80%.

Figure 1 shows one possible layout configuration of the Phase 2 tracker. It will be composed of an Inner Tracker based on silicon pixel modules, and of an Outer Tracker made from silicon modules with strip and macro-pixel sensors.

In this layout, the Inner Tracker has four barrel layers and eleven end-cap disks. Different pixel sizes in the Inner Tracker modules are under consideration, either $25 \times 100 \, \mu m^2$ or $50 \times 50 \, \mu m^2$, which will reduce the pixel area by a factor of about six compared to the current CMS pixel detector. For the studies in this paper, the $25 \times 100 \, \mu m^2$ Inner Tracker modules have been simulated. The Outer Tracker has six barrel layers and five end-cap disks, where a part of the modules in the three innermost barrel layers are arranged in a tilted scheme. The Outer Tracker modules have been designed to provide useful information also at the first trigger level, allowing to maintain its acceptance rate below 100 kHz. Each module is a stack of two closely spaced sensors and is able to correlate hits produced in the two sensors in real time, thereby rejecting low-$p_T$ particles using the strong bending power of the 3.8 T magnetic field. Two different kinds of modules for the final configuration of the Outer Tracker are under study: in the inner layers, macro pixel–strip (PS) modules composed of a bottom sensor with $1.5 \, mm \times 100 \, \mu m$ pixels and a top sensor with $2 \times 25 \, mm$ strips ($100 \, \mu m$ pitch); in the outer layers, strip–strip (2S) modules composed of two sensors with $2 \times 5 \, cm$ long strips ($90 \, \mu m$ pitch) each.

### 3 Track reconstruction method

The CMS track reconstruction algorithm is based on an iterative approach [2]. The main idea is to search for easier-to-find tracks first, to mask the hits associated to the found tracks, and to proceed to the next iteration. In this way the combinatorial problem is reduced, and the search for more difficult classes of tracks is simplified. Moreover, this approach introduces the possibility of developing special iterations that can improve track reconstruction in high-density environments such as jets, or to use the information from other subsystems such as muon chambers and calorimeters.

In each iteration, the so-called Combinatorial Track Finder is run. It can be divided into four different steps:
1. **Seed generation**: Using the information of three or four hits, the trajectory parameters and the corresponding uncertainties of the initial track candidates are computed.

2. **Track finding**: The current trajectory parameters are extrapolated to the next layer and possible compatible hits are found. Each of them is added to a clone of the track candidate. This step is repeated until more than one hit is missing or there are no more tracker layers.

3. **Track fitting**: The best possible estimates of the trajectory parameters at the *impact point*\(^1\) is obtained using a final Kalman or Gaussian-sum filter plus the corresponding smoothers.

4. **Track selection**: Tracks are grouped in different classes (*Loose, Tight* or *High Purity*) according to various track quality cuts.

Although the track density is lower in the Outer Tracker, primary seeding in the Inner Tracker has the following advantages: even at very high pile-up, cluster merging is very much reduced thanks to the high granularity and the concomitant small channel occupancy; the Inner Tracker produces 3-D measurements that provide more constraints and better estimates of the initial trajectory parameters; the efficiency of the reconstruction of low momentum particles that do not cross the entire Outer Tracker is improved. The same seeding algorithm used in the present CMS tracking is also used for Phase 2: triplets are found by purely combining pixel hits in different layers, while quadruplets are created by the so-called “triplet propagation”, which consists in propagating triplets to the next layer, finding possible compatible hits, computing the total \(\chi^2\) and rejecting hits above a certain \(\chi^2\) threshold. The seeding performance has been proved to have high efficiency with relatively low fake rate in realistic simulation studies.

The list of the tracking iterations can be found in Table 1. The main difference between iterations is the configuration of the seed generation and the target tracks. The seeding capability of the Outer Tracker is not yet exploited in the current Phase 2 track reconstruction; this topic is discussed in more detail in Section 5.

\(^1\)The impact point is defined as the point of closest approach of the track to the assumed beam axis.

---

**Figure 1.** *R*-\(z\) view of a possible layout of the new CMS tracker foreseen for Phase 2. The inner part is composed of silicon pixel modules (yellow and light blue), while the outer part is composed by two different kind of silicon modules: PS modules (dark blue) and 2S modules (red).
Table 1. List of the six tracking iterations used in Phase 2, with the corresponding seeding configuration used and the target tracks.

| Iteration | Step Name          | Seeding         | Target Track               |
|-----------|--------------------|-----------------|-----------------------------|
| 0         | HighPtQuadruplet   | pixel quadruplets | prompt, high $p_T$          |
| 1         | HighPtTriplet      | pixel triplets  | prompt, high $p_T$          |
| 2         | DetachedQuadruplet | pixel quadruplets | displaced                  |
| 3         | LowPtQuadruplet    | pixel quadruplets | prompt, low $p_T$          |
| 4         | LowPtTriplet       | pixel triplets  | prompt, low $p_T$          |
| 5         | Muon inside-out    | muon-tagged tracks | muon tracks                |

4 Performance

4.1 Track reconstruction and parameters resolution

In order to assess the track reconstruction performance, defining the association between reconstructed and simulated tracks is particularly important. In the standard CMS definition, a reconstructed track is considered associated to a simulated particle if at least 75% of its hits originate from this simulated particle. If this is not the case, the reconstructed track is considered as a random combination of hits and marked as a fake track. The tracking efficiency is therefore defined as the fraction of charged particles associated to at least one reconstructed track, while the fake rate is the fraction of the fake tracks in the set of reconstructed tracks. Both efficiency and fake rate strongly depend not just on the algorithms and track selections used, but also on the intrinsic tracker properties, such as its layout, its material budget and the precision of its measurements.

The performance of the track reconstruction is evaluated using two different simulated samples. Where needed, a pile-up of minimum-bias events is superimposed, where the number of pile-up events is drawn from a Poisson distribution with mean equal to 140 or 200. The results are shown for the High Purity track selection and can be considered a conservative lower limit and are expected to improve with careful tuning of the reconstruction and matching algorithms for the high pile-up scenario.

The first sample considered consists of events with top quark pair production ($t\bar{t}$) and is used to assess the performance for a typical proton-proton collision at the HL-LHC. Figure 2 shows the results for this sample in both pile-up scenarios. In the top row on the left, the tracking efficiency for particles with $p_T > 0.9$ GeV is plotted as a function of the pseudorapidity, while on the right the rate of fake tracks with $p_T > 0.9$ GeV is shown. The efficiency is around 90% falling off at $|\eta| > 3.8$, while the fake rate is smaller than 5% in the entire range of $\eta$ for pile-up 140. The small loss in efficiency around $\eta = 1.2$ is partially due to the pixel configuration and will be fully recovered by extending the seeding to the Outer Tracker. In the bottom row efficiency and fake rate are plotted as a function of the transverse momentum. The tracking efficiency is around 90% in the range between 1 GeV and 100 GeV, and the fake rate is smaller than 10% below 10 GeV with 140 pile-up events on average. As most particles in the $t\bar{t}$ events are hadrons, the deterioration of the efficiency at high $p_T$ can be explained by the production of secondary particles in inelastic processes, which are very close to the mother particle at high energies and mislead the pattern recognition. With higher pile-up, the efficiency is not affected, while the fake rate almost doubles, but is still tolerable. Figure 3 shows the contribution of the individual iterations to the final tracking efficiency of $t\bar{t}$ events with pile-up 140. Thanks to the iterations targeting low transverse momentum particles, the efficiency is at least 30% above 300 MeV/c.

The second sample consists of single muons, generated according to a flat $\eta$ distribution in the range $|\eta| < 4.0$, with fixed transverse momenta of 10 GeV. It is used to test the tracking performance...
Figure 2. Tracking efficiency (left) and fake rate (right) as a function of the pseudorapidity (upper row) and as a function of the transverse momentum (lower row) for $\bar{t}$ events simulated for the Phase 2 detector with superimposed pile-up collisions of 140 (full circles) and 200 (open circles). Tracks passing the High Purity quality requirements and produced less than 3.5 cm from the centre of the beam spot in radial direction are used. The performance as a function of $\eta$ is for generated particles with $p_T > 0.9$ GeV.

as a function of the pseudorapidity and to determine the resolution of the estimated track parameters at the impact point. In the CMS convention the five trajectory parameters are: $d_0$, the transverse impact parameter; $z_0$, the longitudinal impact parameter; $\phi$, the track angle in the transverse plane; $\cot \theta$, the cotangent of the polar angle; and $p_T$, the transverse momentum. The resolution of track parameters is given by the RMS of the residuals, i.e. the difference between the estimated and the simulated track parameters. Figure 4 shows the tracking efficiency for single muons with a transverse momentum of 10 GeV in both pile-up scenarios. It can be seen that the single muon efficiency is independent of the amount of pile-up. Figure 5 shows the resolution of the five parameters for single muons with $p_T = 10$ GeV as a function of the pseudorapidity for both the current tracker and the future Phase 2
tracking. The resolution deteriorates for large $\eta$ for all parameters, but for different reasons: the shorter lever arm for the estimation of the curvature and of the azimutal angle $\phi$; the larger extrapolation distance from the innermost hit to the beam axis for the impact parameter; and the parametrization of the polar angle $\theta$ by $\cot \theta$. In all five parameters, the resolution is considerably better with the Phase 2 tracker. In particular, a significantly improved $p_T$ resolution can be achieved thanks to the reduction of the material budget and a better hit resolution. Also the transverse impact parameter resolution is much better than with the Phase 1 detector, ranging from below 10 $\mu$m in the barrel region to about 20 $\mu$m in the very forward region.

Figure 3. Tracking efficiency of individual iterations for the $t\bar{t}$ sample with an average pile-up of 140, reconstructed with the Phase 2 detector. The label of each iteration identifies the seeding algorithm used (see Table 1).

Figure 4. Tracking efficiency as a function of the pseudorapidity for single muons with $p_T$ equal to 10 GeV and pile-up of 140 (full circles) and 200 (open circles).
4.2 Signal vertex reconstruction and resolution

The Phase 2 vertex reconstruction [2] is based on the current algorithm used in the present CMS tracker. It proceeds in two steps: first, the vertices are found as clusters of tracks coming from the same interaction point using the Deterministic Annealing algorithm [3]; then, for each found vertex, an Adaptive Vertex Fit [4] computes the best estimate of the vertex position and of the parameters of the associated tracks without using any information on the beam position. Finally, the reconstructed vertices are sorted to identify the signal vertex among the pile-up vertices. The vertex sorting is based on the $\sum p_T^2$. In the case of jets, the individual tracks contributing to the $\sum p_T^2$ are replaced by jets obtained by clustering tracks originating from the same vertex. The final $\sum p_T^2$ is computed using these jets, the remaining isolated single tracks and the missing transverse momentum, re-weighed accordingly. A more detailed description of the sorting method can be found in Ref. [1].

The probability of reconstructing the signal vertex and to tag it correctly is an important figure of merit, and it is strongly correlated with the amount of pile-up in the event. For $t\bar{t}$ events, the efficiency of the correct signal vertex identification is 94% with 140 pile-up events, and 89% with 200 pile-up events. The quality of the vertex reconstruction is also shown in Figure 6. On the left, the number of reconstructed vertices as a function of the number of simulated vertices is shown. The dependence is almost linear. On the right, the merging rate, i.e. the probability of two adjacent vertices to merge into a single one, is shown as a function of their distance in the $z$ coordinate. The merging rate drops to zero at about 0.6 mm both with 140 and with 200 pile-up events. Note that the merging rate is smaller than one even at distances below 25 $\mu$m.

Another important aspect is the resolution of the vertex position in the $x$, $y$ and $z$ coordinates, which is shown in Figure 7 as a function of the number of tracks associated to the vertex. It can be seen that the resolution of the vertex position is almost independent of the amount of pile-up in the event. Moreover, the longitudinal resolution is only 50% worse than the transverse one, as expected given the pixel dimensions of Inner Tracker modules.

As in the case of the tracking performance, all results should be considered as a lower limit of the expected performance.

5 Future developments

Here some developments are listed that are envisaged for further improvement of the CMS Phase 2 tracking:

- **Tracking@HLT using GPUs**: The software for the CMS High-Level Trigger (HLT) tracking has been moved in 2017 from a one-event-per-thread strategy to a many-threads-per-event approach. This massive parallelism within each event scales with the pile-up by offloading the combinatorics to as many threads as are available. This task has been implemented in CMS designing a high-level trigger based on GPUs. The same valid approach will be used also for the future Phase 2 HLT.

- **Tracking in the Outer Tracker**: Many developments are made possible by this new kind of detector. For example, the L1 track trigger information can be used directly in the offline reconstruction for instance to create seeds from L1 tracks or to incorporate L1 algorithms in the offline tracking. Also, the modules of the new Outer Tracker can be used to build short track segments (vector hits) reconstructed from compatible hits in the two sensors of a module, which contain not only position information but also direction information. Algorithms are under development that exploit this information for seeding in the Outer Tracker and for searching for displaced tracks without using pixel information.
• **Multiple algorithms**: This exploits the concept of using different algorithms specialized for certain tasks in different iterations.

• **Iterations targeting physics objects**: As already mentioned in Section 3, the iterative approach is very suitable for introducing special iterations targeting specific physics objects. This has already been tested in the current CMS tracking, but has not yet been fully introduced into the Phase 2 reconstruction sequence. Some examples are the muon specific iterations and the reconstruction of tracks inside jet cones, which makes identification of physics objects more robust, and significantly increases the track reconstruction efficiency and purity [5].

**References**

[1] D. Contardo, M. Klute, J. Mans, L. Silvestris, J. Butler (CMS), CERN-LHCC-2015-010, LHCC-P-008, CMS-TDR-15-02 (2015)

[2] The CMS Collaboration (CMS), JINST **9**, P10009 (2014)

[3] K. Rose, Proceedings of the IEEE **86/11**, 2210 (1998)

[4] R. Frühwirth, W. Waltenberger, P. Vanlaer, Tech. Rep. CMS-NOTE-2007-008, CERN, Geneva (2007), https://cds.cern.ch/record/1027031

[5] The CMS collaboration, https://twiki.cern.ch/twiki/bin/view/CMSPublic/HighPtTrackingDP
Figure 5. Comparison of the resolution, as a function of pseudorapidity, of the five track parameters for the current (black) and the upgraded (red) tracker for single, isolated muons with transverse momenta of 10 GeV. From top to bottom and left to right: transverse and longitudinal impact parameters, $\phi$, $\cot \theta$ and $p_T$. 
Figure 6. Number of reconstructed (“Reco”) vertices versus the number of simulated vertices (left) and merging rate of vertices as a function of their distance in the z coordinate (right) for \( \bar{t} \bar{t} \) events with 140 superimposed pile-up events (full circles) and 200 pile-up events (open circles).

Figure 7. Vertex position resolution in \( x \) and \( y \) (left) and \( z \) (right) as a function of the number of tracks associated to the vertex, for \( \bar{t} \bar{t} \) events with 140 pile-up events (full circles) and 200 pile-up events (open circles).