2D Runout Modelling of Hillslope Debris Flows, Based on Well-Documented Events in Switzerland

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Abstract: In mountain areas, mass movements, such as hillslope debris flows, pose a serious threat to people and infrastructure, although size and runout distances are often smaller than those of debris avalanches or in-channel-based processes like debris floods or debris flows. Hillslope debris-flow events can be regarded as a unique process that generally can be observed at steep slopes. The delimitation of endangered areas and the implementation of protective measures are therefore an important instrument within the framework of a risk analysis, especially in the densely populated area of the alpine region. Here, two-dimensional runout prediction methods are helpful tools in estimating possible travel lengths and affected areas. However, not many studies focus on 2D runout estimations specifically for hillslope debris-flow processes. Based on data from 19 well-documented hillslope debris-flow events in Switzerland, we performed a systematic evaluation of runout simulations conducted with the software Rapid Mass Movement Simulation: Debris Flow (RAMMS DF)—a program originally developed for runout estimation of debris flows and snow avalanches. RAMMS offers the possibility to use a conventional Voellmy-type shear stress approach to describe the flow resistance as well as to consider cohesive interaction as it occurs in the core of dense flows with low shear rates, like we also expect for hillslope debris-flow processes. The results of our study show a correlation between the back-calculated dry Coulomb friction parameters and the percentage of clay content of the mobilised soils. Considering cohesive interaction, the performance of all simulations was improved in terms of reducing the overestimation of the observed deposition areas. However, the results also indicate that the parameter which accounts for cohesive interaction can neither be related to soil physical properties nor to different saturation conditions.

Keywords: hillslope debris flow; RAMMS; 2D runout simulation; cohesive interaction; Switzerland

1. Introduction

Mountain areas are especially prone to flow and slide processes of different mass movements because of their high relief energies. In Switzerland, about eight percent of land area in the country is affected by landslides, often classified as hillslope debris-flow events [1]. To reduce the damage to people and infrastructure caused by hillslope debris-flow events, endangered areas have to be known and mitigation measures are necessary. To this end, initiation areas of shallow slides and associated hillslope debris flows can often be reliably identified, e.g., in [2–5]. However, knowledge of the runout and lateral deposition of such flows is essential. 2D runout simulation models have proven to be suitable tools for creating detailed delineation of typical mass movement deposits in torrent catchments, e.g., in [6–11], supporting the development of hazard maps and the estimation
of process parameters for the design of protective measures [12]. However, the a priori estimation of process parameters as well as the magnitude of hillslope processes is typically associated with large uncertainties.

Following the definition of Hungr et al. [13], a hillslope debris flow is a sensitive clay flowslide or a gravel/sand/debris flowslide of partially or fully saturated debris, spontaneously triggered by excess pore pressure or liquefaction of the sliding material. Hillslope debris flows are secondary processes, typically following translational landslides at slope angles between 20 to 45° [14–17] with initial landslide thicknesses of 0.5 to 2 m [14]. Similar to debris flows, hillslope debris flows show a sharply defined front and border but travel unconfined on open slopes with velocities from 3 m min$^{-1}$ up to 5 m s$^{-1}$ [13]. They either enter torrents or they come to rest on hillslopes, in one or more lobes. Very often these processes do not show a clear transition area, but the trigger area often merges seamlessly into the deposition area, i.e., erosion or mass bulking seems to play a minor role in hillslope debris-flow processes. The stopping process can generally be described as deceleration and lateral spreading. When the water partially drains from the landslide mass, it can cause a decrease in pore pressure with a consequent increase in effective shear resistance, allowing the flow to come to rest [1,16,18].

In this study, we applied the simulation software RAMMS:Debris Flow (DF) to estimate the runout of hillslope debris-flow processes. The numerical simulation tool RAMMS is indented to assist practitioners and researchers to simulate gravitationally-driven natural hazards (avalanches, debris flows and hillslope debris flows) within one single software environment [19]. For this reason, the physical specification in RAMMS can reflect the complex behaviour of the considered process only in a limited way. An essential implication, regarding debris-flow like mass movements, is the assumption of a single-phase mixture. The dynamic behaviour of debris flows and hillslope debris flows is mainly driven by its water content, the ratio of fine to coarse particles in the flow, and possibly also the degree of agitation induced by the interaction of the flow with the rough channel bed [1,20]. Iverson [16], for instance, proposed different dimensionless parameters that characterise the flowing mixture of debris flows. However, these controlling factors are variable within any given flow and between individual debris-flow events, resulting in a substantially variability of data on viscosities of debris-flow events in nature [21,22]. The challenge applying continuum-based dynamical models is therefore the selection of an appropriate flow rheology or of the constitutive equations of the material behaviour and the estimation or calibration of the key model parameters, e.g., [23–25]. For these reasons, simple constitutive concepts, based on either few or easily ascertainable parameters, have their justification in determining the runout or for hazard delineation of mass movements.

RAMMS DF is based on a depth-averaged 2D solution to the implemented law of motion over 3D topography and was originally developed for predicting the runout of snow avalanches. In principal, RAMMS uses the Voellmy–Salm fluid flow continuum model [26,27], which describes the considered flowing mass of snow or debris as an hydraulic depth average continuum model. RAMMS accounts for topographical conditions by assuming a fixed Eulerian 3D coordinate system in $z(x,y)$. Flow is moved in an unsteady and nonuniform motion, characterised by the flow height $H(x,y,t)$ and the mean velocity $U(x,y,t)$ at time $t$ [9,28]. Mass balance is described by

$$\frac{\partial H}{\partial t} + \frac{\partial (HU_x)}{\partial x} + \frac{\partial (HU_y)}{\partial y} = Q(x,y,t)$$

(1)

with $Q(x,y,t)$, denoting the rate of either mass-gaining (entrainment) or mass-loosing (deposition). The momentum of the flow, is described as the balance between acceleration $S_x$ and deceleration (frictional resistance) $S_f$ with

$$S_{gx} - S_{fx} = \frac{\partial (HU_x)}{\partial t} + \frac{\partial \left(c_x HU_x^2 + g_s K_H H^2 \right)}{\partial x} + \frac{\partial (HU_x U_y)}{\partial y}$$

(2)
and

\[ S_{gy} - S_{fy} = \frac{\partial (HU_y)}{\partial t} + \frac{\partial (HU_x U_y)}{\partial x} + \frac{\partial \left( c_g H U_y^2 + g z K H^2 \right)}{\partial y} \tag{3} \]

Details of the governing differential equations are described in Christen et al. [28]. RAMMS uses the total variation diminishing (TVD) finite volume scheme (FVM) applied on 3D terrain [29]. By this method, averaged cell values are calculated for each place in a grid by means of the edge fluxes from the neighbouring cells.

Frictional resistance is given by the Voellmy-type shear stress [30], a concept combining a dry Coulomb friction term (defined by \( \mu \)) with the velocity-dependent Chezy friction term (defined by \( \xi \)):

\[ S_f = \mu N + \frac{\rho g U^2}{\xi} \tag{4} \]

Here, \( \rho \) denotes the bulk density of the flow, \( U \) the flow velocity, \( N \) the normal pressure and \( g \) the acceleration due to gravitational attraction.

Regarding the dry Coulomb friction, it is customary to scale the shear stress \( S \) linear with the normal pressure \( N \) (i.e., the flow height), assuming a constant parameter \( \mu \) (c.f. the first term on the right side in Equation (4)). However, experiments with dense snow avalanches have shown that the strength of the cohesive binding between particles in the flow disproves such a linear relationship, i.e., a constant friction parameter \( \mu \) [31,32].

When applying RAMMS DF on hillslope debris-flow events, Christen et al. [19] reported markedly different back-calculated friction coefficients compared to those used for channelised debris flows. Hillslope debris flows seem to show a pronounced coherent viscoplastic flow behaviour [1,33,34]—a rheological property similar to dense snow avalanches. For these reasons, a nonlinear relationship between normal pressure and shear stress might be assumable for such processes as well. RAMMS DF accounts for such a viscoplastic flow behaviour, i.e., the influence of cohesive interaction at low shear rates, by modifying the dry Coulomb friction criteria. This allows a rapid increase of the shear stress at low normal pressures (small flow heights) up to a user defined normal pressure threshold (\( N_0 \)), which defines the location of the inflection point of the shear curve [35].

\[ S_f = \mu N + (1 - \mu) N_0 - (1 - \mu) N_0 \exp \left( -\frac{N}{N_0} \right) + \frac{\rho g U^2}{\xi} \tag{5} \]

Note that in the case of \( N >> N_0 \), the nonlinear term in Equation (5) converges to 0, and thus again corresponds to Equation (4). Bartelt et al. [36] therefore denote \( N_0 \) as yield stress of the flow and \( \mu \) as “hardening” parameter. Nevertheless, \( N_0 \) is not a third independent friction value, but rather an additional kinetic parameter, which is intended to better reflect a more cohesive flow behaviour. This new approach apparently improves the accuracy of runout prediction for snow avalanches [35] and has also been applied to simulate debris-flow events based on a physical modelling approach [37]. However, it has not yet been tested for application to hillslope debris flows.

The objective of this study was to perform a systematic evaluation of RAMMS DF simulations based on 19 well-documented hillslope debris-flow events occurring in 2002 in the Appenzell and 2005 as well as 2012 in the Entlebuch and Eriz regions of Switzerland. All simulations have been carried out with and without consideration of cohesive interaction. After describing the compiled event data, the evaluation concept and the constellation of applied friction parameters, the predicted runout zones compared to the observed runout areas and different parameter settings as well as their performances are discussed.
2. Methods

2.1. Hillslope Debris-Flow Events

In total, data of 19 well-documented hillslope debris-flow events in Switzerland were used for this study. For each event, we collected information about the geographical location, the slope of the failure surface, its length, width, thickness and volume, as well as the total travel distance (inclined distance from the highest point of the release area to the lowest point of the main deposition area). Data on soil classification had not been documented previously and were determined for 16 events used in this study. Based on sieve and hydrometer analysis, the definition of the Atterberg limits, the soil classification and grain size distribution could be identified. Having determined the prevailing soil class for each event, general key values such as the equivalent friction angle or effective soil cohesion (or yield stress of the soil) have been derived.

The compiled events occurred 2002 in the regions of Appenzell (Canton of Appenzell-Ausserrhoden), 2005 in Entlebuch (Canton of Lucerne) and 2012 near Eriz (Canton of Bern). The soils in Appenzell and Entlebuch were already strongly saturated by previous rainfall events. In contrast, the events in the region of Eriz were triggered without prior saturation [38,39]. All events used in this study have been described in detail by Rickli and Bucher [40], Rickli et al. [41] and Steinemann [38]. The location and dimensions of the triggering areas were therefore known due to GPS coordinates provided by the authors mentioned above and visible on the additionally used aerial images “SwissImage”. Also, the run-out distances were known due to the event documentations [38,40,41]. For the region of Eriz, the run-out areas were mapped by Steinemann [38] whereas for the events in Entlebuch and Appenzell, aerial images where used to determine the run-out areas for this study. Figure 1, shows two examples of the hillslope debris-flow events used for this study.

![Figure 1](image)

Figure 1. Release area (R) and deposition zone (D) of two of the documented hillslope debris-flow events used for this study [42]. A transition area is not clearly identifiable. Both events occurred in 2005 in Entlebuch (Canton of Lucerne, Switzerland).

An overview of all the events and the selected process parameters is given in Table 1.
Table 1. Characteristics of 19 hillslope debris-flow events in the regions of Appenzell (2002), Entlebuch (2005) and Eriz (2012) in Switzerland, based on event documentations [38,40,41] and soil analysis. The equivalent friction angle refers to the mean gradient of the flow path, estimated from the distal limits of the source area and deposit of the observed event.

| Event ID | Volume [m$^3$] | Total Distance [m] | Travel Distance [m] | Equivalent Friction Angle [$^\circ$] | USCS Soil Class | Clay Content [%] |
|----------|----------------|-------------------|---------------------|------------------------------------|-----------------|------------------|
|          |                |                   |                     |                                    |                 |                  |
| **Appenzell, saturated soil conditions assumed** | | | | | | |
| 1003     | 60             | 43                | 23                  | CL                                 | 16.0            |                  |
| 1005     | 130            | 84                | 22                  | CL                                 | 16.0            |                  |
| 1007     | 800            | 105               | 22                  | CL                                 | 16.0            |                  |
|          |                |                   |                     |                                    |                 |                  |
| **Entlebuch, saturated soil conditions assumed** | | | | | | |
| 3001     | 378            | 147               | 19                  | SC                                 | 12.0            |                  |
| 3004     | 280            | 109               | 22                  | SC - SM                            | 8.9             |                  |
| 3005     | 918            | 208               | 19                  | SC                                 | 8.1             |                  |
| 3007     | 960            | 130               | 22                  | CL                                 | 14.8            |                  |
| 3011     | 392            | 114               | 24                  | SC                                 | 14.8            |                  |
| 3015     | 175            | 53                | 29                  | CM                                 | 24.0            |                  |
| 3017     | 1050           | 114               | 18                  | SC                                 | 12.3            |                  |
| 3021     | 153            | 53                | 18                  | GM                                 | 12.0            |                  |
| 3028     | 2800           | 170               | 16                  | -                                  | -               |                  |
| 3029     | 380            | 121               | 21                  | ML, $\eta > 30$                    | 15.1            |                  |
|          |                |                   |                     |                                    |                 |                  |
| **Eriz, unsaturated soil conditions assumed** | | | | | | |
| HM1      | 100            | 119               | 18                  | -                                  | -               |                  |
| HM4      | 112            | 72                | 23                  | CM                                 | 15.5            |                  |
| HM5      | 91             | 124               | 21                  | SM                                 | 8.0             |                  |
| HM6      | 42             | 175               | 26                  | GC - GM                            | 0.8             |                  |
| HM7      | 108            | 136               | 26                  | -                                  | -               |                  |
| HM24     | 655            | 152               | 25                  | GC                                 | 9.0             |                  |

2.2. Evaluation Concept

To quantify the accordance between simulated and observed deposition area, we used the evaluation concept proposed by Heiser et al. [43]. This concept enables an objective comparison and visualisation of model performance across platforms that is independent of process type. The proposed method is based on the comparison of normalised partial observed and simulated areas of deposition (Figure 2), which can be plotted in a ternary diagram to visualise the degree of over- and underestimation. Results are summarised in the single value $\Omega_T$:

$$\Omega_T = \alpha_T - \beta_T - \gamma_T$$  \hspace{1cm} (6)

where $\alpha_T$ is overlap calculated as $X/T$, $\beta_T$ is underestimation calculated as $U/T$ and $\gamma_T$ is overestimation as $O/T$ (see Figure 2 for definitions of $O$, $U$, $X$ and $T$). Referring to a receiver operating characteristic (ROC) approach, as, for instance, is applied to analyse the susceptibility of landslide [44] and debris flows [45], $X$ could be defined as the true positives, $U$ as the false negatives and $O$ as the false positives. However, the true negatives are not clearly definable, as the true negatives depend on the simulation perimeter, which is not clearly demarcable—hindering a comparison of the simulation performance of different events. The evaluation concept, based on Equation (6), has the advantage that the possible range of $\Omega_T$ is fixed between 1 (indicating a perfect fit) and $-1$ (total misfit), regardless of the simulation perimeter.
Figure 2. Schematic mass movement deposit distribution with superimposed simulation. \( A \) is the observed deposition area (reference situation), whereas \( \hat{A} \) is the total simulated area. \( O \) is the size of the overestimated area, whereas \( U \) is the size of the underestimated area. \( X \) is the area in which the simulation outcome and the reference situation overlap. Finally, \( T \) refers to \( A \cup \hat{A} \).

For this study, we applied the evaluation concept to find those friction parameters which are best reproducing the observed deposition area by applying the parameter settings described in Section 2.3. In other words, we performed multiple simulations until the largest \( \Omega_T \) value for each event and each setting was found.

2.3. Parameter Settings

The aim of this study was to investigate whether the modified Voellmy–Salm model (VS model, Equation (5)) leads to significant improvements in the prediction of the runout behaviour of hillslope debris flows. For this reason, all compiled events were back-calculated based on the standard Voellmy-type shear stress model, defined by \( \mu \) and \( \xi \) (cf. Equation (4)). No yield stress of the flow was considered for these simulations. To compare the standard VS with the modified VS model, further simulations were performed with the modified shear stress Equation (5)—taking into account the shear stress of the flow \( N_0 \) as the only calibration parameter. Here, the parameters of the standard Voellmy model were kept constant. The simulations presented in this study are based on the following three parameter settings:

A Back-calculation of best-fit friction parameters \( \mu^* \) and \( \xi^* \) without applying a yield stress of the flow \( N_0 \).

B Back-calculation of a best-fit yield stress of the flow \( N_0^* \) by using mean friction parameters \( \langle \mu^* \rangle \) and \( \langle \xi^* \rangle \) from simulations based on setting A for each study area (Appenzell, Entlebuch and Eriz).

C Back-calculation of a best-fit yield stress of the flow \( N_0^{**} \) by using default values of \( \mu = 0.2 \) and \( \xi = 200 \) as proposed by the user manual for RAMMS DF [46].

A classic backward calculation is based on the setting A, where the best-fit Voellmy parameters \( \mu^* \) and \( \xi^* \) were determined.

Setting B applies the mean Voellmy-type shear stress values as given from setting A (\( \mu^* \) and \( \xi^* \)) to calibrate \( N_0^* \), the effective yield stress of flow. Finally, default Voellmy-type shear stress values were used in setting C to explore a possible simple method, accounting for the yield stress of the flow \( N_0^{**} \) as the only user defined friction parameter in RAMMS DF.

3. Results

A main challenge for simulation models with a physical background is, besides the selection of suitable flow resistance parameters, the definition of an appropriate stopping criteria. In this study, we defined the stopping criteria of the RAMMS DF simulations for each region individually during the first scenario simulations and kept them constant for all subsequent runs. The flow in the model is considered to stop when the percentage of the mass momentum drops below a small constant value which is referenced to the maximum calculated momentum of the flow. The use of such a cut-off
momentum criterion increases the objectivity of using the model because the flow often creeps forward at a very low rate (a few cm/s) when it would otherwise be judged to stop when visualising the results.

The stopping criterion for simulations in Entlebuch and Eriz belong to 3.3% and 6.2% of the maximum calculated momentum. Those stopping criteria were defined based on the events Entlebuch-3001 and Eriz-HM1, because they involved undisturbed runout on a uniform slope. Using the default parameters $\mu = 0.2 \text{ [-]}$ and $\xi = 200 \text{ [m/s}^2\text{]}$, suggested by Bartelt et al. [46], the stopping criteria with the best visual match between the documented and the modelled runout area was chosen. With only three events observed in Appenzell, we applied a constant stopping criteria, which belongs to 5% of the maximum calculated momentum. When running the model, it was assumed that the initial flow starts instantaneously and not as a progressive failure with a series of smaller-volume slumps.

The best-fit values for all parameter settings and hillslope debris-flow events are listed in Table 2.

It is remarkable that the back-calculated velocity-dependent friction parameters $\xi$ of hillslope debris-flow events follow a narrower bandwidth than the dry Coulomb friction criteria in the modelling of hillslope debris-flow events. An example of back-calculated results for all parameter settings of the event HM4 (Eriz)—compared to the observed runout zone—is shown in Figure 3.

**Table 2.** Back-calculated resistance values for all parameter settings used in this study.

| Event ID | Setting A | Setting B | Setting C † |
|----------|-----------|-----------|-------------|
|          | $\mu^*$ \[\] | $\xi^*$ \[m/s$^2\] | $N_0^*$ \[kPa\] | $\langle \mu^* \rangle$ \[\] | $\langle \xi^* \rangle$ \[m/s$^2\] | $N_0^*$ \[kPa\] |
| Appenzell |           |           |             |
| 1003     | 0.23      | 200       | 0.00        | 0.31      | 200       | 0.10       |
| 1005     | 0.40      | 200       | 0.20        | 0.31      | 200       | 0.70       |
| 1007     | 0.30      | 200       | 0.05        | 0.31      | 200       | 0.25       |
| Entlebuch |           |           |             |
| 3001     | 0.21      | 300       | 0.05        | 0.30      | 507       | 0.05       |
| 3004     | 0.13      | 240       | 0.00        | 0.30      | 507       | 0.00       |
| 3005     | 0.11      | 190       | 0.00        | 0.30      | 507       | 0.00       |
| 3007     | 0.46      | 150       | 1.70        | 0.30      | 507       | 1.60       |
| 3011     | 0.40      | 285       | 1.10        | 0.30      | 507       | 1.55       |
| 3015     | 0.49      | 300       | 2.75        | 0.30      | 507       | 2.95       |
| 3017     | 0.33      | 550       | 0.10        | 0.30      | 507       | 0.60       |
| 3021     | 0.35      | 1250      | 1.35        | 0.30      | 507       | 1.50       |
| 3028     | 0.24      | 700       | 1.10        | 0.30      | 507       | 0.78       |
| 3029     | 0.33      | 1100      | 0.65        | 0.30      | 507       | 0.95       |
| Eriz     |           |           |             |
| HM1      | 0.20      | 400       | 0.00        | 0.23      | 446       | 0.05       |
| HM4      | 0.37      | 175       | 0.30        | 0.23      | 446       | 0.30       |
| HM5      | 0.05      | 300       | 0.00        | 0.23      | 446       | 0.00       |
| HM6      | 0.05      | 200       | 0.00        | 0.23      | 446       | 0.00       |
| HM7      | 0.40      | 900       | 0.19        | 0.23      | 446       | 0.17       |
| HM24     | 0.29      | 700       | 0.65        | 0.23      | 446       | 1.20       |
† all simulations with $\mu = 0.20$ and $\xi = 200$, following RAMMS user manual [46].
Figure 3. Simulation results of hillslope debris-flow event HM4 (Eriz) for all parameter settings. Observed release area and runout zone are shown with red and blue lines, respectively.

Typical $\mu$ and $\xi$ parameters for different mass movements are plotted in Figure 4 along with the best-fit Voellmy-type friction parameters of the compiled hillslope debris-flow events used in this study (Setting A).
3.1. Back-Calculation of Friction Parameters $\mu$ and $\xi$ (Setting A)

For the setting A, all events could be simulated, estimating the best-fit Voellmy-type shear stress parameters $\mu$ and $\xi$ without considering the yield stress of flow.

On average, nearly 50% of depositional zones, predicted by simulations based on the parameter setting A, agree with the observed deposition areas documented in Rickli and Bucher [40], Rickli et al. [41] and Steinemann [38]. However, most simulations also considerably overestimated the lateral spread of the flow, compared to field observations. This is reflected by the large $\gamma_T$ value in Table 3. The overall performance in predicting hillslope debris-flow deposition zones based on simulations with setting A, can be given quantitatively with an $\Omega_T$ value of $-0.05 \pm 0.18$ (cf. Table 3).
Table 3. Evaluation results for setting A. $\alpha_T$ denotes the simulation performance related to the overlap (a value of 1 corresponds to full coverage of simulation/observed). $\beta_T$ is a performance measure of the underestimation, whereas $\gamma_T$ shows the overestimation performance of the considered simulation. The overall performance is specified by $\Omega_T$. All values are calculated based on Equation (6), following the procedure described in Heiser et al. [43].

| Setting A | $\alpha_T$ | $\beta_T$ | $\gamma_T$ | $\Omega_T$ |
|-----------|------------|------------|------------|------------|
| **Appenzell** | | | | |
| mean value | 0.49 | 0.03 | 0.48 | -0.02 |
| standard deviation | 0.06 | 0.02 | 0.04 | 0.12 |
| **Entlebuch** | | | | |
| mean value | 0.48 | 0.07 | 0.45 | -0.04 |
| standard deviation | 0.10 | 0.08 | 0.09 | 0.20 |
| **Eriz** | | | | |
| mean value | 0.45 | 0.03 | 0.52 | -0.10 |
| standard deviation | 0.09 | 0.04 | 0.10 | 0.17 |
| **Overall** | | | | |
| mean value | 0.47 | 0.05 | 0.48 | -0.05 |
| standard deviation | 0.09 | 0.07 | 0.09 | 0.18 |
| sample count | 19 | 19 | 19 | 19 |

3.2. Back-Calculation of Cohesion Parameters $N_0^*$ and $N_0^{**}$ (Settings B and C)

Settings B and C have been set up to analyse the simulation performance of RAMMS DF as a function of the yield stress of the flow only. For this reason, we kept the Voellmy-type shear stress parameters $\mu$ and $\xi$ constant.

For parameter setting B we applied the back-calculated mean friction values of parameter setting A for each study site and calibrated event-specific yield stresses of the flow $N_0^*$. The calibrated yield stress values of the flow for all events have been found to range between 0.00 and 2.75 kPa (Table 2), and the mean performance evaluation value for all simulations conducted with setting B amounts to $\Omega_T = -0.05 \pm 0.24$ (Table 4).

For parameter setting C, we applied the default friction values $-\mu = 0.2$ and $\xi = 200$—as proposed by Bartelt et al. [46], which resulted in back-calculated yield stress values of the flow ($N_0^{**}$), ranging from 0.00 to 2.95 kPa (cf. Table 2).
Table 4. Evaluation results for settings B and C. $\alpha_T$ denotes the simulation performance related to the overlap (a value of 1 corresponds to full coverage of simulation/observed). $\beta_T$ is a performance measure of the underestimation, whereas $\gamma_T$ shows the overestimation performance of the considered simulation. The overall performance is specified by $\Omega_T$. All values are calculated based on Equation (6), following the procedure described in Heiser et al. [43].

| Setting | $\alpha_T$ | $\beta_T$ | $\gamma_T$ | $\Omega_T$ | $\alpha_T$ | $\beta_T$ | $\gamma_T$ | $\Omega_T$ |
|---------|------------|-----------|------------|-----------|------------|-----------|------------|-----------|
| Appenzell | mean value 0.48 | 0.09 | 0.43 | -0.04 | 0.51 | 0.03 | 0.46 | 0.02 |
|          | standard deviation | 0.03 | 0.07 | 0.09 | 0.07 | 0.06 | 0.02 | 0.04 | 0.12 |
| Entlebuch | mean value 0.46 | 0.16 | 0.38 | -0.08 | 0.50 | 0.10 | 0.40 | 0.01 |
|          | standard deviation | 0.14 | 0.15 | 0.11 | 0.29 | 0.11 | 0.09 | 0.10 | 0.22 |
| Eriz | mean value 0.51 | 0.12 | 0.36 | 0.03 | 0.52 | 0.11 | 0.37 | 0.04 |
|          | standard deviation | 0.10 | 0.11 | 0.15 | 0.21 | 0.11 | 0.11 | 0.14 | 0.22 |
| Overall | mean value 0.48 | 0.14 | 0.38 | -0.04 | 0.51 | 0.09 | 0.40 | 0.02 |
|          | standard deviation | 0.12 | 0.13 | 0.12 | 0.24 | 0.10 | 0.11 | 0.11 | 0.21 |
| sample count | 19 | 19 | 19 | 19 | 19 | 19 | 19 | 19 |

The average performance of setting C ($\Omega_T = 0.02 \pm 0.24$) is higher than those of setting A and setting B. This might be due to lower overestimation $\gamma_T$ and better accordance $\alpha_T$, despite a similar increased underestimation $\beta_T$ (c.f. Figure 5).

Figure 5. Graphical displays to compare the resulting $\Omega_T$ values for the simulation settings A and B (left figure) and A and C (right figure). The right and left increasing colour ranges indicate increasing over- or underestimation of performance ($\gamma_T, \beta_T > 30\%$). Weak performance is defined by $\alpha_T < 40\%$ and $\gamma_T, \beta_T > 30\%$.

4. Discussion and Conclusions

Basically, the overall simulation performance of settings A–C do not differ significantly. Approximately 50% of the observed deposition area is predicted by all simulation settings. We therefore conclude that an additional calibration of $N_0$ does not provide sufficient evidence for a fundamental improvement of the simulation performance. However, in combination with default $\mu$
and $\xi$ values, the yield stress of the flow could be applied as the only user defined flow resistance parameter. Therefore, we see potential, by applying the concept of internal cohesive bonding, especially when it leads to a reduced number of parameters that have to be calibrated.

Simulations based on fixed $\mu$ and $\xi$ values and only calibrating the yield stress of the flow $N_0$—settings B and C—showed 10% and 8% less overestimation of the observed depositional area, respectively. Visually this performance improvement can be seen in Figure 5.

The overall performance values $\Omega_T$ for setting B and C is more centralised compared to the related performance values of setting A. Interestingly, the simulation performance does not change significantly even when default friction parameters $\mu$ and $\xi$ (Setting C) are assumed. For inverse modelling reasons, the slight improvement (of overestimation) in predicting the deposition area with parameter settings B and C may motivate future research to consider yield stress of the flow for simulating runout of hillslope debris-flow events, whereas both back-calculated yield stress values of the flow are in a similar range as those empirically found for dense snow avalanches based on snow-chute experiments [31,32,35] (see Table 5).

| Process                  | $\langle N_0 \rangle$ [kPa] | $\langle \mu \rangle$ [ ] | Study                      |
|--------------------------|-----------------------------|---------------------------|----------------------------|
| wet snow experiments †   | 0.665 ± 0.688               | 0.41 ± 0.08               | [35]                       |
| dry snow experiments †   | 0.194 ± 0.140               | 0.30 ± 0.11               | [35]                       |
| hillslope debris flows   | 0.536 ± 0.735               | 0.28 ± 0.04               | this study, setting B      |
| hillslope debris flows   | 0.671 ± 0.773               | 0.20 ± 0.00               | this study, setting C      |

† based on snow chute experiments conducted by Platzer et al. [31,32].

Berger et al. [37] analysed functionality and robustness for rare and extreme debris flows that could not be modelled in the laboratory, by using RAMMS DF applying a constant yield stress of the flow. They reported their best-fit parameter combination, predicting both the debris flow velocities and flow heights, with $\mu = 0.00$, $\xi = 600$ m/s$^2$ and $N_0 = 0.5$ kPa. Because their best-fit simulations showed no influence of the dry Coulomb friction parameter ($\mu = 0.00$), they suggested that in the channel the debris is fluidized and the flow is well lubricated.

One might further hypothesise that different saturation conditions, which affect shear strength in the soil, might potentially also affect cohesive interaction of the bulk mixture at low shear rates. Our results, however, indicate that the pre-saturation of the soil does not play a significant role for the simulation of the compiled hillslope debris-flow events with RAMMS DF, because we could not detect any clear differences in the simulation performance between the field sites. Further, the yield stress of the flow $N_0$ does not correlate with the effective cohesion $c'$, i.e., the shear stress independent of the normal stress—typically also denoted as yield stress in soil mechanics (Figure 6).
Effective cohesion $c'$ [kPa]

Yield stress of the flow $N_0$ [kPa]

Setting B $\langle N_0 \rangle = 0.98$ kPa

Setting C $\langle N_0\rangle^* = 0.89$ kPa

On the other hand, the back-calculated dry Coulomb friction values $\mu^*$ show a substantially clear correlation with the percentage clay content in the soil (Figure 7). The same trend can be observed for the yield stress of the flow values $N_0^*$ and $N_0^{**}$. These findings support the results of Hürlimann et al. [1]. They observed that the clay content strongly influenced the runout distance and the affected area of experimental hillslope debris flows in the laboratory.

Considering forward modelling, where constitutive parameters have to be known or plausibly assumed, our results show that the yield stress of the flow $N_0$ cannot be determined either by the degree of saturation or by the static yield stress of the soil. A strong correlation, however, can be shown between the dry friction parameter $\mu$ respectively yield stress of the flow $N_0$ and the clay content of the soil.

The numerical simulation program RAMMS intends to offer an easy-to-calibrate tool for the risk delimitation of mass movements. This of course also implies a reduction of the physical basis for the description of complex processes. A reason why the strength of RAMMS cannot be found in a near-natural modelling of the considered process but in a plausible simulation of dynamic prototypical quantities, which form an essential basis for a hazard assessment. Especially for the depositional area of debris-flow-like processes, it has become obvious that beside rheological properties, the topographical conditions have a significant influence on the flow heights, flow velocities and thus on the runout distances.

In any case, note that specifically for hillslope debris flows, runout simulations are based on further assumptions. One uncertainty refers to the estimation of the precise position and size of the release area, which often has a strong influence on simulation results owing to local variations in
topography. Furthermore, the consideration of cohesive binding between particles as an additional shear stress represents a strong simplification of the forces acting within a moving mass. Finally, the deposition pattern of a simulation depends on the user-selected stopping criterion. Because the stopping of a hillslope debris flow depends on interactions between fluid and solid components, which are often highly heterogeneous, defining the correct stopping criterion is a problem not yet solved in one component models of the runout of mass movements [60]. It appears that the stopping criterion is also likely to be influenced by the dissolution of the underlying DEM. However, a sensitivity analysis in this respect was outside the scope of this study.

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