FORMATION OF HIGH-REDSHIFT (z > 6) QUASARS DRIVEN BY NUCLEAR STARBURSTS

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Received 2009 July 1; accepted 2009 October 9; published 2009 November 4

ABSTRACT

Based on the physical model of a supermassive black hole (SMBH) growth via gas accretion in a circumnuclear disk (CND) proposed by Kawakatu & Wada, we describe the formation of high-z (z > 6) quasars (QSOs) whose BH masses are $M_{\text{BH}} > 10^9 M_\odot$. We derive the necessary conditions to form QSOs at z > 6 by only gas accretion: (1) a large mass supply with $M_{\text{sup}} > 10^{10} M_\odot$ from host galaxies to CNDs, because the final BH mass is only 1%–10% of the total supplied mass from QSO hosts. (2) High star formation efficiency for a rapid BH growth which is comparable to high-z starburst galaxies such as submillimeter galaxies. We also find that if the BH growth is limited by the Eddington accretion, the final BH mass is greatly suppressed when the period of mass supply from hosts, $t_{\text{sup}}$, is shorter than the Eddington timescale. Thus, the super-Eddington growth is required for the QSO formation while $t_{\text{sup}}$, which is determined by the efficiency of angular momentum transfer, is shorter than $\sim10^8$ yr. The evolution of the QSO luminosity depends on the redshift $z_i$ at which accretion onto a seed BH is initiated. In other words, the brighter QSOs at $z > 6$ favor the late growth of SMBHs (i.e., $z_i \approx 10$) rather than early growth (i.e., $z_i \approx 30$). For $z_i \approx 10$, $t_{\text{sup}} \approx 10^8$ yr is shorter than that of the star formation in the CND. Thus, the gas in the CND can accrete onto a BH more efficiently, compared with the case for $z_i \approx 30$ (or $t_{\text{sup}} \approx 10^9$ yr). Moreover, we predict the observable properties and the evolution of QSOs at $z > 6$. In a QSO phase, there should exist a stellar rich massive CND, whose gas mass is about 10% of the dynamical mass inside $\sim0.1$–1 kpc. On the other hand, in a phase where the BH grows (i.e., a proto-QSO phase), the proto-QSO has a gas-rich massive CND whose gas mass is comparable to the dynamical mass. Compared with the observed properties of the distant QSO SDSS J1148+5251 observed at $z = 6.42$, we predict that SDSS J1148+5251 corresponds to the scenario of the late growth of SMBH with $z_i \approx 10$, which is accompanied by a massive CNDs with $M_\phi \approx 5 \times 10^{10} M_\odot$ and the luminous nuclear starburst $L_{\text{IR}}$ at infrared band with $L_{\text{IR}} \approx 10^{47}$ erg s\(^{-1}\). Moreover, we predict that the progenitor of SDSS J1148+5251 can be the super-Eddington object. These predictions can be verified by ALMA, SPICA, and JWST.

Key words: black hole physics – early universe – galaxies: active – galaxies: nuclei – galaxies: starburst – ISM: structure

Online-only material: color figures

1. INTRODUCTION

Supermassive black holes (SMBHs) with masses in the range of $10^9$–$10^{10} M_\odot$ are the engines that power active galactic nuclei (AGNs) and quasars (QSOs). There is also ample evidence that SMBHs reside at the center of most galaxies (e.g., Kormendy & Richstone 1995; Richstone et al. 1998; Ho 1999), including the Milky Way (e.g., Genzel et al. 1997; Schödel et al. 2002; Ghez et al. 2003). In the local universe, there are tight correlations between the masses of SMBHs and the masses and velocity dispersions of the spheroidal components (bulge) of the hosts (e.g., Kormendy & Richstone 1995; Richstone et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000; Tremaine et al. 2002; Marconi & Hunt 2003; Häring & Rix 2004; Barth et al. 2005). These observational facts suggest that an intriguing link between the formation of bulges and SMBHs.

High-redshift QSOs are essential to understand the formation and evolution of SMBHs. In recent years, more than thirty QSOs at $z \approx 6$ have been discovered (Fan et al. 2000, 2001, 2003, 2004, 2006; Goto 2006; Jiang et al. 2006; Willott et al. 2007; Jiang et al. 2009). The higher luminosity of the distant QSO at $z = 6.42$, corresponding to SDSS J1148+3251 (Fan et al. 2003) with $10^{47}$ erg s\(^{-1}\), implies that a SMBH with mass $\gtrsim10^9 M_\odot$ is already in place within $\sim1$ Gyr after the big bang, by assuming the Eddington luminosity. These requirements set significant constraints on the evolution and formation of SMBHs in the early universe. There are some analytical and semi-analytical studies (Haiman & Loeb 2001; Haiman 2004; Yoo & Miralda-Escudé 2004; Shapiro 2005; Volonteri & Rees 2006; Tanaka & Haiman 2009) and numerical simulations (Li et al. 2007; Sijacki et al. 2009) that discuss the formation of $>10^9 M_\odot$ SMBH at $z > 6$. A key physical process governing evolution of QSOs is the mass accretion toward a SMBH, although BH growth via merging may be expected at the high mass BH with $M_{\text{BH}} > 10^9 M_\odot$ (e.g., Shankar 2009 and references therein). Although the accretion process is a complicated phenomenon over 9 orders of magnitude in the size scale, the Eddington-limited accretion rate was simply assumed in most previous studies. However, the evolution of the SMBH is not only controlled by the accretion processes in the vicinity of the SMBH, but also related to the mass supply from the host galaxy to the circumnuclear region.

A number of mechanisms for gas accumulation on the $\sim1$–1 kpc scale down to the galactic central region have been proposed, e.g., the tidal torque driven by the major and minor mergers of galaxies (e.g., Toomre & Toomre 1972; Mihos &...
Hernquist 1994, 1996; Saitoh & Wada 2004; Saitoh et al. 2009) and the stellar bars (e.g., Noguchi 1988; Shlosman et al. 1990; Fukuda et al. 1998; Fukuda et al. 2000; Maciejewski et al. 2002; Namekata et al. 2009), gas drag and dynamical friction in the dense stellar cluster (Norman & Scoville 1988) and the radiation drag (e.g., Umemura et al. 1997; Umemura 2001; Kawakatu & Umemura 2002). However, the accumulated gas does not directly accrete onto a SMBH, since the angular momentum of the gaseous matter cannot be thoroughly removed. Thus, some residual angular momentum would terminate the radial infall, so the accreted gas forms a reservoir, i.e., a circumnuclear disk (CND), in the central ~100 pc around a SMBH whose scale depends on the angular momentum of the gas. If the gravitational instability takes place in a CND, star formation is naturally expected in this region. Active nuclear star formation (~100 pc) has been actually observed in nearby AGNs (e.g., Imanishi & Wada 2004; Davies et al. 2007; Watabe & Umemura 2005; Ballantyne 2008; Schartmann et al. 2008; Wada et al. 2009). The nuclear starburst also affects the growth of SMBHs, because the radiation and/or supernova (SN) feedback from starbursts can enhance the mass accretion onto a SMBH (e.g., Norman & Scoville 1988; Umemura et al. 1997; WN02; Vollmer & Beckert 2003; Vollmer et al. 2008; Collin & Zahn 2008). In order to reveal the final rate of mass accretion to the BH region, it is crucial to link mass accretion processes from a galactic scale with those from an accretion disk in the vicinity of a central BH, via the CND. Recently, we have proposed a theoretical model of a nuclear starburst disk supported by the turbulent pressure led by SN explosions (Kawakatu & Wada 2008; hereafter KW08). In KW08, the turbulence excited by SN transports the angular momentum. We showed how a SMBH grows from a seed BH, taking into account the mutual connection between the mass supply from a host galaxy and the physical states of the CND accompanied by the star formation. This theoretical model should be confirmed for the formation of high-z (z > 6) QSOs whose masses are \( \gtrsim 10^9 M_\odot \).

This paper is organized as follows. We briefly outline the model in KW08 in Section 2. By adopting KW08, we will show the necessary conditions to form QSOs at z > 6 in terms of the total accreted gas mass from host galaxies and star formation efficiency in the CNDs (Section 3). In addition, we will predict observable properties and the evolution of QSOs at z > 6 (Section 4). In Section 5, we discuss how the distant QSO J1148+5251 at z = 6.42 forms and predict the nature of the early phase of this QSO. Section 6 is devoted to our summary. Unless otherwise stated, all results shown below refer to the currently favored cold dark matter (DM) model with \( \Omega_M = 0.24, \Omega_\Lambda = 0.76, h = 0.73, \sigma_8 = 0.042, n = 0.95 \) (Spergel et al. 2007).

2. MODELS

We here briefly describe a coevolution model of SMBHs and CNDs (KW08). We assume that dusty gas is supplied to a region around a central SMBH at a constant rate of \( \dot{M}_{\text{sup}} \) from a host galaxy whose surface density \( \Sigma_{\text{host}} \), including the gas and stellar components (Figure 1 in KW08). The accumulated gas forms a clumpy CND around a central SMBH with \( M_{\text{BH},\text{ini}} \), which is vertically supported by turbulent pressure via SN explosions (WN02; Vollmer & Beckert 2003; Vollmer et al. 2008; Collin & Zahn 2008). We here assume the isothermal cold gas dominates mass (\( T_g = 50–100 \) K) in the CND since the molecular and dust cooling is effective (e.g., Wada & Tomisaka 2005; Wada et al. 2009).

2.1. Turbulent Pressure-supported CND

On the vertical structure of the CND, we assume that the turbulent pressure associated with SN explosions is balanced to gravity, \( g \) caused by

\[
\rho_g(r) v_t^2(r) = \rho_g(r) g(r) h(r),
\]

where \( \rho_g(r), v_t(r), \) and \( h(r) \) are the gas density, the turbulent velocity, and the scale height of the disk, respectively. Here, the gravity, \( g(r) \) is obtained as \( g(r) \equiv GM_{\text{BH}}/r^2 + \pi G (\Sigma_{\text{disk}} + \Sigma_{\text{host}}) \), where \( \Sigma_{\text{disk}}(r) \) is the surface density of baryonic components (the gaseous matter and stars). The geometrical thickness is determined by the balance between the turbulent energy dissipation and the energy input from SN explosions as follows.

\[
\frac{\rho_g(r) v_t^2(r)}{t_{\text{dis}}(r)} = \frac{\rho_g(r) v_t^2(r)}{h(r)} = \eta_{\text{SN}} S_\ast(r) E_{\text{SN}},
\]

where the dissipation timescale of the turbulence \( t_{\text{dis}}(r) = h(r)/v_t(r) \), \( E_{\text{SN}} \) is the total energy \( (10^{51} \text{erg}) \) injected by an SN, and \( \eta_{\text{SN}} \) is heating efficiency per unit mass which denotes how much energy from SNe is converted to kinetic energy of the matter. Recent observational studies on the relationship between star formation rate and gas surface density in nearby galaxies suggest that the star formation rate is approximately proportional to the gas density for high-density regions \( (n_H > 10^2 \text{cm}^{-3}) \), i.e., \( S_\ast = C_\ast \rho_g^n \) with \( n \sim 1 \) (e.g., Bigiel et al. 2008). Here \( C_\ast \) is the star formation efficiency. Theoretical studies based on numerical simulations of the interstellar medium (ISM) also support this proportionality for the high-density end (Wada & Norman 2007; Dobbs & Pringle 2009; Krumholz et al. 2009). Since we are interested in the evolution of dense CNDs with \( n_H > 10^2 \text{cm}^{-3} \), we here suppose \( S_\ast = C_\ast \rho_g \).

The star formation timescale \( t^\ast = 1/\dot{M}^\ast \) is of the order of an orbital period in a quasi-steady, self-regulated galactic disk,
in which the Toomre Q-value is roughly unity. However, observations suggest that the local star formation rate for a given gas density varies widely distributed by one to two orders of magnitude (Komugi et al. 2005; Bigiel et al. 2008; see also Figure 5 and discussion in Section 3.1). Based on a theoretical model of the ISM and star formation, Wada & Norman (2007) claimed that this wide variety could be caused by a wide range of star formation efficiency. In general, the star formation rate (or efficiency) on small scale is not simply determined only by gas density (see, e.g., Kawamura et al. 2009 for molecular clouds in LMC). The physical background of this variety is still unclear even in our Galaxy. This is also the case in the galactic central region. Although many local spiral galaxies show molecular gas concentration in the central sub-kpc region (e.g. Komugi et al. 2008), the star-forming activity is not uniquely determined by the gas density. In fact, the local star formation rate is correlated with a fraction of high-density molecular gas (Muraoka et al. 2009). Moreover, at high redshift, the star formation efficiency in the galactic central region is hardly determined observationally and theoretically. The circumnuclear gas disk is not necessarily in a self-regulated state, since the rotational timescale is comparable to the lifetime of massive stars or smaller. Therefore under frequent mergers of small gas-rich galaxies at high redshift, which would be a main cause of mass supply toward a galactic center, the circumnuclear region might be far from an equilibrium. Considering all these uncertainties, we here assume that the star formation timescale is a free parameter, and examine the results for a wide range of $C_c$.

By using Equations (1) and (2), $v_i(r)$ and $h(r)$ can be obtained (see also Equations (4) and (5) in KW08). For given $r$ and $M_{BH}$, it is found that $v_i \propto C_{\ast}^{1/2}$ and $h \propto C_{\ast}^{1/2}$ (see also WN02). The velocity dispersion of molecular hydrogen in CNDs is in fact positively correlated with the star formation rate (Hicks et al. 2009).

2.2. Two Modes of Gas Accretion in CND

We suppose a kinetic viscosity as a source of angular momentum transfer in the gas disk. Then, the mass accretion rate in a viscous accretion disk is given by

$$M(r) = 2\pi v_i(r)\Sigma_g(r) \left| \frac{d \ln \Omega(r)}{d \ln r} \right|, \quad (3)$$

where the viscous parameter is $v_i(r) = \alpha v_i(r) h(r)$, $\Sigma_g$ is the surface density of the gas component in the CND, and the angular velocity $\Omega(r)$ is given by the radial centrifugal balance. Here $\alpha(\leq 1)$ is a constant in time. The inner radius of the CND ($r_{in}$) is determined by the dust sublimation radius, i.e., $r_{in} = 3pc(M_{BH}/10^9M_{\odot})^{1/2}$ (see KW08 for details). At $r_{in}$ we assume the CND connects with the steady accretion disk. With respect to the stability, we adopt Toomre’s stability criterion, i.e., when the surface density of gas in the CND, $\Sigma_g$ is higher (lower) than the critical surface density, $\Sigma_{crit}$ the CND is gravitationally unstable (stable). The critical surface density is obtained as $\Sigma_{crit}(r) = \kappa(r)c_s/\pi G$, where $\kappa(r) \equiv 4\pi^2G(2\Omega^2(r)d\Omega(r)/dr)^{1/2}$ is the epicyclic frequency and $c_s$ is the sound velocity. The critical radius $r_c$ is determined by the Toomre criterion, that is, $\Sigma_g(r_c) = \Sigma_{crit}(r_c)$. In this picture, we naturally expect two modes of gas accretion rate as follows. Mode (i): if $r_c < r_{in}$ (i.e., the CND is fully gravitationally unstable), then the CND is geometrically thick due to SN energy feedback, and as a result we have a large accretion rate. We here suppose $a_{SN} = 1$ motivated by numerical simulations demonstrated by WN02.

Mode (ii): if $r_c > r_{in}$, the scale height of the inner region would be much smaller than mode (i), because the scale height is determined by the thermal pressure, $P_g(r) = \rho_g(r)h(r)$, where $P_g(r) = \rho_g(r)c_s^2$. Here $c_s = (5kT_g/3\mu_p)^{1/2}$, where $k$ and $\mu_p$ are the Boltzmann constant and the proton mass. In mode (ii), the magneto-rotational instability could be a source of turbulence, but the turbulent velocity is comparable to or even smaller than the sound speed (e.g., Balbus & Hawley 1991; Machida et al. 2000). As a result, the accretion is less efficient than the mode (i). We assume $a_{MRI} = 0.5$ and $\alpha = \alpha_0$ in mode (ii). Note that the adopted $a_{MRI} = 0.5$ is relatively larger than that derived by numerical simulations (e.g., Machida et al. 2000), but we confirmed that the following results do not change at all, even if we use smaller $a_{MRI}$ (e.g., $a_{MRI} = 0.01$).

2.3. Coevolution of SMBHs and CNDs

Our main purpose is to evaluate the growth of SMBHs, the star formation rate, and gas mass in the CND. We here focus on the time dependence of characteristic radius in the disk ($r_c$, $r_{in}$, and $r_{out}$), instead of solving the evolution of radial structure of CND. The radial surface density distribution of CND is assumed to be $\Sigma_{disk}(r) = \Sigma_{disk,0}(r/r_{out})^{-\gamma}$ where $r_{out}$ is the outer radius of the CND. Hereafter, we assume $\gamma = 1$ although the dependence of $\gamma$ on $M_{BH}$ is weak for $0 < \gamma < 2$ (see Section 3.2 in KW08). In this model the gas supplied from the host galaxy is eventually consumed to form the SMBH and stars. Thus, the time evolution of the gas mass in the disk, $M_g(t) = \int_{r_{in}}^{r_{out}} 2\pi r^2 \Sigma_g(r')dr'$, is simply given by the mass conservation:

$$M_g(t) = \int_0^t \left[ M_{sup}(\tau') - M_e(\tau') - M_{BH}(\tau') \right] d\tau', \quad (4)$$

where $M_{sup}(t)$, $M_e(t)$, and $M_{BH}(t)$ are the mass supply rate from hosts, the star formation rate, and the growth rate of SMBHs, respectively. Here we ignore the mass loss from stars and from CNDs due to the starburst wind. The time evolution of SMBH mass $M_{BH}(t)$ is obtained as $M_{BH}(t) = M_{BH,seed} + \int_0^t M_{sup}(\tau')d\tau'$, where we assume the mass of seed BHs, $M_{BH,seed} = 10^2M_{\odot}$, as end-products of the first generation stars (e.g., Fryer et al. 2001; Heger et al. 2003; Omukai & Palla 2003; Yoshida et al. 2006). For $M_{sup}$, we can assume any function for the mass supply rate, but here we simply take a step function as the first attempt as $M_{sup}(t) = \text{const}$ for $t < t_{sup}$, while $M_{sup}(t) = 0$ for $t > t_{sup}$ where $t_{sup}$ is a period of the mass supply from host galaxies. Thus, key parameters of the SMBH growth and the state of CNDs are $M_{sup}$, $t_{sup}$, and $C_c$.

The growth rate of SMBHs, i.e., $\dot{M}_{BH}$, is not necessarily equal to the mass accretion rate at the inner boundary, $M(r_{in})$. The growth rate could be limited by the Eddington accretion rate, $\dot{M}_{edd}$ where $\dot{M}_{edd} \equiv L_{edd}/c^2$ and $L_{edd} = 4\pi c G M_{BH}m_p/\sigma_T$ with $\sigma_T$ being the Thomson cross section. However, based on radiation hydrodynamic simulations, it is also claimed that $\dot{M}_{BH} > \dot{M}_{edd}$, i.e., super-Eddington accretion, could be possible since both the radiation field and mass accretion flow around a SMBH is non-spherical (Ohsuga et al. 2005; Ohsuga 2007; Ohsuga & Mineshige 2007). Thus we here consider two possible models for $\dot{M}_{BH}$.

(i) $\dot{M}_{BH} = \dot{M}(r_{in})$. \quad (5)

The BH grows with a super Eddington rate if $\dot{M}(r_{in}) > \dot{M}_{edd}$.

(ii) $\dot{M}_{BH} = \dot{M}_{edd}$. \quad (6)
where $\epsilon_{\text{BH}} = 0.1$ is the energy conversion efficiency. We here assume that there is a mass “outflow” with a rate, $M_{\text{outflow}} = M(\tau_{\text{in}}) - M_{\text{BH}}$. Hereafter we call the model (i) and model (ii) as the super-Eddington growth model and the Eddington-limited growth one, respectively. We first show results of the super-Eddington accretion in Sections 3.1 and 4.1. Results based on the Eddington-limited accretion are discussed in Sections 3.2 and 4.2.

Finally, we should stress what happens if we use the nonlinear Kennicutt–Schmidt’s law, i.e., $S = C'\rho_g^{-1}\rho_g^{1.5}$, where $t_{ff}$ is the free-fall timescale. It is found that the BH growth rate is then described by $M_{\text{BH}} \propto C'\rho_g^{-1} \propto M_*$ because of the turbulent viscosity $v_t \propto C'$, while the star formation rate scales as $M_s \propto M_0^2$. Thus, the gas supplied from host galaxies turns into stars in the CND more efficiently, compared with the case for $S \propto \rho_g$ (see Equation (4)). It implies that the final BH mass becomes smaller due to the efficient star formation, if we adopt nonlinear Kennicutt–Schmidt’s law.

3. NECESSARY CONDITIONS OF FORMATION OF SMBHs AT $z > 6$

Based on the coevolution model of CNDs and SMBHs (Section 2 and KW08), we examine conditions of the formation of SMBHs with $M_{\text{BH}} \geq 10^9 M_\odot$ at $z > 6$. We first show results of the super-Eddington growth model in Section 3.1, and those of the Eddington-limited growth model in Section 3.2.

3.1. Super-Eddington Growth Model

Figure 1 shows the final BH mass, $M_{\text{BH,final}}$, as a function of the total mass accreted from hosts, $M_{\text{sup}}$ for the different period of mass supply from hosts, $t_{\text{sup}}$ assuming $C_\star = 3 \times 10^{-8}$ yr$^{-1}$. This value is comparable to the star formation efficiency of high-$z$ galaxies (e.g., Tacconi et al. 2006; see also Figure 5). The effect of $C_\star$ will be discussed below. The red lines are the results of the super-Eddington growth model for $t_{\text{sup}} = 10^5$ yr, $10^6$ yr, and $10^9$ yr. The blue line denotes that all the supplied mass is used to grow the SMBH, i.e., $M_{\text{BH,final}} = M_{\text{sup}}$. It is found that $M_{\text{BH,final}} \approx (0.01 - 0.1) M_{\text{sup}}$. This low efficiency is independent of the period of the mass supply from hosts, $t_{\text{sup}}$ and the mass supply rate of hosts, $M_{\text{sup}}$. In order to form SMBHs with $M_{\text{BH}} > 10^9 M_\odot$, plenty of infalling gas from host galaxies, i.e., $M_{\text{sup}} > 10^9 M_\odot$ is requested. We consider why the mass ratio, $M_{\text{BH,final}}/M_{\text{sup}}$, is too small as we showed. From the BH growth rate for the high accretion rate (Section 2.2 and see also Equation (12) in KW08), the accretion energy onto a central BH, i.e., $0.5M_{\text{BH}}v_m^2$ where $v_m = \sqrt{GM_{\text{BH}}/r_m}$, can be obtained as

$$\frac{1}{2} M_{\text{BH}}v_m^2 = 2f_\gamma \alpha_{\text{SN,SN}} E_{\text{SN}} M_\star,$$

(7)

where $f_\gamma \equiv [3(14 - 4 \gamma)(8 - 4 \gamma)/16(\gamma/160h)^2 - 2$. Thus, Equation (7) indicates that $\alpha_{\text{SN}}$ and $E_{\text{SN}}$ are important parameters to determine the conversion efficiency from the energy input from SN explosions ($\approx E_{\text{SN}} M_\star$) to the accretion energy onto a central BH ($\approx M_{\text{BH}}v_m^2$). Using the fiducial values of $\gamma = 1$, the ratio of the SMBH growth and star formation rate of CNDs is given by

$$M_{\text{BH}}/M_\star = 0.3 \alpha_{\text{SN}} \left(\frac{E_{\text{SN}}}{10^{-3} M_\odot}\right) \left(\frac{M_{\text{disk}}}{10^8 M_\odot}\right)^{-0.5}.$$  

(8)

This indicates that larger $M_{\text{sup}}$ (or $M_{\text{disk}}$) leads to smaller $M_{\text{BH,final}}/M_{\text{sup}}$. This can be understood as follows. As $M_{\text{sup}}$ becomes larger $M_{\text{BH}}$ increases. The larger BH mass causes a smaller scale height and a smaller turbulent velocity because the CND is vertically supported by the turbulent pressure (Equation (1)). Thus, the growth rate of BHs ($\propto v_t \propto v_\text{in}$) decreases as $M_{\text{sup}}$ (or $M_{\text{disk}}$) is larger. Note that $M_{\text{disk}}$ is basically determined by two quantities, i.e., $\alpha_{\text{SN}}$ and $E_{\text{SN}}$ which control turbulent viscosity and efficiency of SN heating, respectively.

Next, we examine the dependence of the star formation efficiency, $C_\star = M_*/M_\odot$, on the mass of SMBHs, $M_{\text{BH}}(t)$. Figure 2 shows the evolution of the SMBH mass, $M_{\text{BH}}(t)$, for the different star formation efficiency, $C_\star$. We here assume the total mass accreted from hosts, $M_{\text{sup}} = 10^{11} M_\odot$ and a period of the mass supply from hosts, $t_{\text{sup}} = 10^9$ yr. The redshift $z_i$ when the accretion onto a seed BH got started is supposed to be $z = 25$. Thus, the growth timescale of SMBHs must be less than $8 \times 10^5$ yr (vertical dot-dashed line) to form the SMBH at $z > 6$. The allowed region to form a SMBH with $M_{\text{BH}} > 10^9 M_\odot$ at $z > 6$ is shown as shaded. We find that $M_{\text{BH}}(t)$ significantly depends on the star formation efficiency, $C_\star$. If the star formation efficiency is extremely low (e.g., $C_\star \approx 3 \times 10^{-9}$ yr$^{-1}$), the timescale of SMBH growth is larger than the Hubble time at $z = 0$ because of $t_{\text{growth}} \approx r_m^2/v_t h \sim (f_\gamma C_\star)^{-1}$ (see Equation (14) in KW08). Thus, $M_{\text{BH,final}}$ cannot be larger than $3 \times 10^{-9} M_\odot$ in order to be satisfied with $M_{\text{BH}} > M_\star$.

4 The numerical simulations have shown $\epsilon_{\text{SN}} \approx 1$ (e.g., WO02). On the other hand, the parameter $\epsilon_{\text{SN}}$ is expressed as $\epsilon_{\text{SN}} = \epsilon_{\text{SN,SN}} f_{\text{SN}}$, where $\epsilon_{\text{SN}}$ and $\epsilon_{\text{SN,SN}}$ are the efficiency with which SN energy is transferred to the gas in the CND, and the number density of SNe per solar mass of the star formation, respectively. In this paper (also in KW08), we assume $\epsilon_{\text{SN,SN}} = 10^{-3} M_\odot^{-1}$, that is, $\epsilon_{\text{SN}} = 0.1$ (e.g., Thornton et al. 1998; Wada & Norman 2002; Wada et al. 2009), and $f_{\text{SN}} = 10^{-2} M_\odot^{-1}$, which is expected for Salpeter initial mass function with low-mass cutoff being $m_1 = 0.1 M_\odot$. Note that the heating efficiency $\eta_{\text{SN}}$ must be larger than $10^{-3} M_\odot^{-1}$ in order to be satisfied with $M_{\text{BH}} > M_\star$.  

Figure 2. Time evolution of the mass of BH for different $C_\star$. The right blue, magenta, green, blue, and red lines correspond to $C_\star = 3 \times 10^{-6}$ yr$^{-1}$, $3 \times 10^{-7}$ yr$^{-1}$, $3 \times 10^{-8}$ yr$^{-1}$, $3 \times 10^{-9}$ yr$^{-1}$, and $3 \times 10^{-10}$ yr$^{-1}$, respectively. Here we assume $M_{\text{sup}} = 10^{11} M_\odot$ and $t_{\text{sup}} = 10^9$ yr. The shaded region represents the allowed region for the formation of SMBHs with $M_{\text{BH}} > 10^9 M_\odot$ at $z > 6$. The dot-dashed vertical line corresponds to $z = 6$ if the redshift $z_i$ at which the accretion onto a seed BH starts is $z_i = 25$. (A color version of this figure is available in the online journal.)
~10^9 M⊙ until z = 6 (the red line in Figure 2). For the extremely high efficiency (e.g., C∗ ~ 3 × 10^{-8} yr^{-1}; light blue line in Figure 2), on the other hand, the gas supplied from the host is mostly consumed by the star formation (M_{sup} ≈ M_∗), thus the final SMBH mass is smaller than 10^9 M⊙. Therefore, in order to form a SMBH with M_{BH} > 10^9 M⊙ at z ~ 6, relatively high star formation efficiency, i.e., 10^{-8} yr^{-1} ≲ C_∗ ≲ 10^{-7} yr^{-1} is required.

We show the evolution of M_{BH}(t) for the case of t_{sup} = 10^8 yr (Figure 3) and t_{sup} = 5 × 10^8 yr (Figure 4), respectively, to elucidate the dependence of a period of the mass supply from hosts t_{sup} on M_{BH}(t). Comparing Figure 2 with Figure 3, the final BH masses for t_{sup} = 10^8 yr are almost the same as that for t_{sup} = 10^9 yr (Figure 2), but the behavior of M_{BH}(t) for t_{sup} = 10^8 yr is different from that for t_{sup} = 10^9 yr at given C_∗ = 3 × 10^{-6} yr^{-1} (the light blue line). This is because for t_{sup} = 10^9 yr the mass supplied rate is higher than the star formation rate (M_{sup} > M_∗). Thus, the final BH mass can be as large as ~10^9 M⊙. As a result, the allowed region is 10^{-8} yr^{-1} ≲ C_∗ ≲ 10^{-6} yr^{-1} for t_{sup} = 10^8 yr. The upper value C_∗ is determined by the local gravitational free-fall timescale, t_{ff} ≈ (G M_*/m_p)^{-1/2} ~ 10^6 yr, for the averaged density of CNDs, i.e., n_{disk} = 10^{-3} cm^{-3}, because of the star formation timescale t_{s} = C_∗^{-1} ≳ t_{ff}. We also found that the required range of C_∗ for t_{sup} = 10^7 yr is the same as those for t_{sup} = 10^8 yr. Figure 4 shows that there is no solution to form the SMBH with M_{BH} > 10^9 M⊙ at z > 6 for t_{sup} = 5 × 10^8 yr because of M_{sup} ≈ M_∗ for the wide range of C_∗, i.e., 3 × 10^{-10} yr^{-1} ≲ C_∗ ≲ 3 × 10^{-9} yr^{-1}. In other words, this indicates the rapid mass supply from the host to the central tens pc region (M_{sup} > 20 M_⊙ yr^{-1}, M_{sup} = 10^{11} M⊙) is also necessary to form the SMBHs at z > 6.

Figure 5 shows the SFR as a function of the surface density of gas in CNDs, Σ_g. We estimate the surface gas density of CNDs as Σ_g = M_g/πr^2. Here we take M_g and r_{out} from our calculations. The size of the CND increases with time but finally r_{out} ≈ 2 × 10^3 pc. For the SFR and Σ_g in the shaded region, SMBHs with M_{BH,final} > 10^9 M⊙ at z > 6 can be formed as a result of considering the dependences of C_∗ and Σ_g. The observational data of nearby normal galaxies (Komugi et al. 2005) and nearby starburst galaxies (Kennicutt 1998) are plotted in Figure 5. The two plots represent the average of massive star-forming submillimeter galaxies (SMGs) at z ~ 2.5 with SFR ~ 10^{-4} M⊙ yr^{-1} pc^{-2} and Σ_g ~ 5 × 10^3 M⊙ pc^{-2} (e.g., Tacconi et al. 2006) and a QSO at z = 6.42 (SDSS J1148) with SFR ~ 10^{-3} M⊙ yr^{-1} pc^{-2} and Σ_g ~ 10^4 M⊙ pc^{-2} (Walter et al. 2009). Note that these values are similar to those of z ~ 4 QSOs (Riechers et al. 2009). The required C_∗ for high-z SMBH formation is comparable to SMGs and QSO hosts at z = 6.42, although this is higher than that of low-z normal galaxies and starburst ones. Thus, the predicted high star formation efficiency, i.e., 10^{-3} yr^{-1} ≲ C_∗ ≲ 10^{-2} yr^{-1} actually occurred in the high-z universe.

In summary, in order to form the high-z SMBH (i.e., z > 6 and M_{BH,final} > 10^9 M⊙) by super-Eddington gas accretion we need (1) abundant mass supply from the galactic scale (~kpc), i.e., M_{sup} > 10^{10} M⊙, (2) rapid mass inflow from the galactic scale (~kpc), i.e., t_{sup} < 5 × 10^8 yr, and (3) high star formation efficiency, i.e., 10^{-8} yr^{-1} ≲ C_∗ ≲ 10^{-6} yr^{-1}. 

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**Figure 3.** Same as Figure 2, but t_{sup} = 10^8 yr. The lines are the same as in Figure 2.

(A color version of this figure is available in the online journal.)

**Figure 4.** Same as Figure 2, but for t_{sup} = 5 × 10^8 yr. The lines are the same as in Figure 2.

(A color version of this figure is available in the online journal.)

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**Figure 5.** Comparison between the observed surface star formation rate (SFR) in terms of the surface gas density (Σ_g) and the allowed region for the formation of SMBHs with M_{BH} > 10^9 M⊙ at z > 6 (the shaded region). The blue lines represent theoretical predictions for different C_∗, assuming M_{sup} = 10^{11} M⊙ and t_{sup} = 10^8 yr. Black filled dots are starburst galaxies in Kennicutt (1998) and the open dots are normal galaxies in Komugi et al. (2005). Green point denotes the average dusty submillimeter galaxies (SMGs) at z ≈ 2.5 (Tacconi et al. 2006) and red point represents ~kpc-scale star-forming region around the z = 6.42 SDSS J1148+5251 (Walter et al. 2009).

(A color version of this figure is available in the online journal.)
3.2. Eddington-limited Growth Model

We here discuss the results of the Eddington-limited growth model (the black lines in Figure 1). Figure 1 shows that the Eddington-limited growth model leads to much lower efficiency for $t_{sup} \approx 10^3$ yr and $10^4$ yr, i.e., $M_{BH, final} / M_{sup}$ equals to $(10^{-3} - 10^{-2}) M_{sup}$. But, the efficiency for $t_{sup} = 10^5$ yr is comparable to that of the super-Eddington growth model, i.e., $M_{BH, final} / M_{sup} \approx 0.01 - 0.1 M_{sup}$. These results can be understood in terms of the ratio of the mass supply timescale, $t_{sup}$ and the Eddington timescale, $t_{Edd} = \rhoBH \sigmaT / (4\pi G \mu_0)$. The black hole grows exponentially at the late time ($t \gg t_{Edd}$) because of $t_{sup} = 10^5$ yr because of $t_{sup} \gg t_{Edd}$. Thus, the final BH mass is comparable to that of the super-Eddington growth model. In order to form a SMBH with $> 10^9 M_{\odot}$, it is found that the super-Eddington growth is needed when $t_{sup}$ is shorter than $\sim 10^9$ yr. Note that the dependence of $C_s$ and $t_{sup}$ on the final BH mass are the same as those for the super-Eddington growth model.

4. OBSERVABLE PROPERTIES AND EVOLUTION OF QSOs AT $z > 6$

Based on the present model in Section 3, we here discuss observable properties and the evolution of QSOs at $z > 6$ in order to compare them with the current and future observations. It is still unclear when the accretion onto a seed BH got started in the high-$z$ universe. Recently, Johnson & Bromm (2007) mentioned that the radiation feedback from the first stars may deplete the gas in the central region of the protogalaxy and may delay the BH accretion by up to $\sim 10^8$ yr. Thus, we explore the relationship between the evolution of QSOs at $z > 6$ and the redshift $z_i$ when the seed BH begins to grow. To this end, we examine the evolution and formation of high-$z$ QSOs at $z > 6$ for the two scenarios of high-$z$ QSO formation: (1) the early growth of SMBHs, i.e., $z_i = 25$. This corresponds to the supply period $t_{sup} = 7 \times 10^8$ yr and (2) the late growth of SMBHs, i.e., $z_i = 8$. This corresponds to the supply period $t_{sup} = 10^8$ yr. We here use the fiducial values, i.e., $M_{sup} = 10^{11} M_{\odot}$ and $C_s = 3 \times 10^{-8}$ yr$^{-1}$, for which a SMBH with $M_{BH} > 10^9 M_{\odot}$ at $z > 6$ can be formed. We define the QSO phase as $t_{sup} < t < t_{QSO}$ where $t_{QSO}$ is the time when the AGN luminosity equals to the threshold luminosity of QSOs, $L_{QSO, th}$. We assume $L_{QSO, th} = 10^{46}$ erg s$^{-1}$. The proto-QSO phase is defined as the early phase of a growing BH ($0 \leq t \leq t_{sup}$).

Figure 6 shows the evolution of the optical depth of CNDs for the UV band in the edge-on view ($\tau(t)$) defined as $\tau(t) = \int_{r_{out}}^{\infty} \chi_d \rho_d \sigma_v (\rho_d) dr \simeq \chi_d M_d(r) / [2 \pi \rho_d \sigma_v (\rho_d) h_{out}(r)]$ where $\chi_d$ is the mass extinction due to the dust and $h_{out}(r)$ is the scale height at $r_{out}(r)$. The mass extinction coefficient $\chi_d$ is given by $\chi_d = n_d \sigma_d / \rho_d$ with the number density $n_d$ and cross section $\sigma_d$. In this paper, we assume $\chi_d = 10^4$ cm$^2$ g$^{-1} (a_d/0.1 \mu m)^{-1} (\rho_d / g$ cm$^{-3}) (Z/Z_{\odot})$, where $a_d$ is the grain radius, $\rho_d$ is the density of solid material density within the grain (e.g., Spitzer 1978), their Section 9.3), and $Z$ is the metallicity of gas, which are fixed at $a_d = 0.1 \mu m$, $\rho_d = 1$ g cm$^{-3}$.

![Figure 6](image-url)
is initiated. In other words, it is easier to build-up bright QSOs if the gas is supplied rather late on a relatively short timescale. This can be understood as follows. For $z_i = 8$, the mass supply timescale, $t_{\text{sup}}$, is shorter than the star formation timescale, $t_s \propto C^{-1}_s$. Thus, the gas in the CNDs can accrete onto a BH more efficiently, compared with the case for $z_i = 25$. In contrast, if the average gas supply rate is smaller in a longer period, (i.e., $z_i = 25$), the supplied gas is mainly consumed to form stars not to form a SMBH because of $t_{\text{sup}} > t_s$.

We also find that the AGN luminosity is sub-Eddington with $L_{\text{AGN}}/L_{\text{Edd}} \approx 0.1$–1 in the QSO phase, while it is super-Eddington with $L_{\text{AGN}}/L_{\text{Edd}} \approx 1$–10 in the proto-QSO phase (see Figures 7(a) and (b)). On the other hand, the luminosity for the QSO phase is comparable to that in the proto-QSO phase. This indicates that the Eddington ratio, $L_{\text{AGN}}/L_{\text{Edd}}$, varies 2 orders of magnitudes for a given AGN luminosity. This implies that the BH mass derived from only AGN luminosity leads to a large uncertainty.

The nuclear starburst (SB) luminosity for the proto-QSO phase is larger than that for the latter half of QSO phase, because the SB luminosity increases with time in the proto-QSO, while it decreases with time in the QSO phase. This trend is prominent for $z_i = 8$ rather than for $z_i = 25$ (see Figure 7(a) and (b)). In this model, the enhanced star formation in a BH growing phase (i.e., a proto-QSO phase) is expected. At low-$z$ universe, Sani et al. (2009) discovered that the star formation activity in narrow line Seyfert galaxies (NLS1s) is larger than that in broad line Seyfert galaxies (BLS1s) of the same AGN luminosity. If NLS1s are the early phase of BLS1s, these observations are consistent with our predictions. We also find that the nuclear SB luminosity is comparable to the AGN luminosity in both the proto-QSO and QSO phases.

The lifetime of QSO is $t_{\text{QSO}} \approx 1 \times 10^8$ yr for $z_i = 25$ and $t_{\text{QSO}} \approx 3 \times 10^8$ yr for $z_i = 8$. These values of $t_{\text{QSO}}$ are consistent with the previous studies (e.g., Martini & Schneider 2003; Martini et al. 2003; Kawakatu et al. 2003; Granato et al. 2004; Shen et al. 2007; Li et al. 2007). From comparison between two models, we find that the QSO phase is longer in more luminous QSOs. We should note that $t_{\text{QSO}}$ is larger for less luminous QSOs, e.g., $t_{\text{QSO}} \approx 2 \times 10^7$ yr (case (a)) and $t_{\text{QSO}} \approx 5 \times 10^7$ yr (case (b)) for $L_{\text{QSO},i0} = 10^{45}$ erg $\text{s}^{-1}$. This has already been pointed out by Hopkins et al. (2005) and Li et al. (2007).

Figure 8 shows the time evolution of the BH mass, $M_{\text{BH}}(t)$, the gas mass in the CND, $M_g(t)$, the stellar mass in the disk, $M_s(t)$, and the total supplied mass from hosts. The evolution of $M_g(t)$ is closely related to that of $L_{\text{AGN}}(t)$ because the CNDs become gravitationally stable as $M_g$ decreases (see Section 2). In the QSO phase, we find that $M_{g}(t) \approx (3–5)M_{\odot} = 5 \times 10^9–1 \times 10^{10} M_{\odot}$, $M_{s}(t) \approx 100 M_{\text{BH}} = 10^4 M_{\odot}$ for $z_i = 25$ (Figure 8(a)), and $M_g(t) \approx (3–30)M_{\text{BH}} = 5 \times 10^8–5 \times 10^9 M_{\odot}$ and $M_s(t) \approx (10–100)M_{\text{BH}} = 10^{10}–10^{11} M_{\odot}$ for $z_i = 8$ (Figure 8(b)). Thus, it is predicted that there exists a stellar rich massive CND around SMBHs, i.e., $M_g \approx 0.1M_{\text{dyn}}$ where $M_{\text{dyn}}$ is the dynamical mass of the CND plus BH system. On the other hand, in the proto-QSO phase it is found that $M_{g}/M_{\text{BH}} \approx 10^{-10}$ for $z_i = 25$ and $M_{g}/M_{\text{BH}} \approx 10^{-2}–10^{-3}$ for $z_i = 8$. Thus, we predict that the proto-QSOs have a gas-rich CND around SMBHs, i.e., $M_g \approx M_{\text{dyn}}$. At late times ($t > 10^8$ yr), a very massive stellar nuclear disk ($M_{\text{star}} \approx 10^{10} M_{\odot}$) remains as a by-product of the formation of SMBHs with $M_{\text{BH}} > 10^6 M_{\odot}$. Since the size of torus ($r_{\text{out}}$) grows up $\sim 2$ kpc in this phase, the circular velocity of stellar components in the CND is $\approx 300 \text{ km s}^{-1}$. This is comparable to the velocity dispersion of giant elliptical galaxies (e.g., Tremaine et al. 2002). Comparing the case of $z_i = 25$ with that of $z_i = 8$, the larger amount of gas in the CND for $z_i = 8$ exists just before the QSO phase (see Figures 8(a) and (b)). As a result, the high mass accretion rate ($M_{\text{BH}}$) is achieved, and the brighter AGN luminosity is sustained for a longer timescale. This is why the QSO lifetime for $z_i = 8$ is longer (see Figure 7(a) and (b)) than that for $z_i = 25$. In addition, for $z_i = 25$ the stellar mass $M_s$ becomes larger than the gas mass $M_g$ at $t_{\text{max}} \approx 10^8$ yr. Thus, the AGN luminosity does not increase after $t_{\text{max}} \approx 10^8$ yr (see Figure 7(a)), even when the gas continues to infall from hosts into CNDs. This supplied gas is mainly consumed to form stars, not to form SMBHs.

Based on the present results, we can predict the observable properties of proto-QSOs as follows: (1) a gas-rich CND with the mass ratio $M_g/M_{\text{BH}} > 10^{-3}$, which is larger than that of QSOs, i.e., $M_g/M_{\text{BH}} \lesssim 10$. (2) The nuclear SB luminosity is slightly higher than that of QSOs. Thus, in order to explore
proto-QSOs, it is essential to estimate the gas and stellar mass in CNDs, and the nuclear SB activity. Jiang et al. (2006, 2009) have recently discovered 2 mag fainter QSOs at $z \sim 6$ than bright QSOs discovered in previous survey (e.g., Fan et al. 2003). Moreover, Kurk et al. (2009) found that two faint QSOs have very narrow broad emission lines (Mg II and C IV), which may imply small BH mass and high Eddington luminosity ratios. Thus, these faint QSOs may be good candidate of proto-QSOs with a super-Eddington mass accretion flow. It is interesting to examine the presence of gas-rich CNDs for these high-$z$ faint QSOs using ALMA. But, we should mention that it is hard to judge whether the proto-QSOs are super-Eddington objects by only these observable properties of CNDs. Thus, we will really need to explore the direct evidence of super-Eddington objects.

4.2. Eddington-limited Growth Model

In Section 4.1, we have shown the evolution of luminosity and mass for the super-Eddington growth model (see Figures 7 and 8). In order to compare with the super-Eddington growth model, we examine these evolutions for the Eddington-limited growth models with $z_i = 8$ (or $t_{\text{sup}} = 10^8$ yr) in Figure 9, and $z_i = 25$ (or $t_{\text{sup}} = 7 \times 10^8$ yr) in Figure 10. Figure 9 (top panel) shows that the peak AGN luminosity is $\sim 10^{45}$ erg s$^{-1}$. This is one order magnitude smaller than the threshold luminosity of QSOs (i.e., $L_{QSO, \text{th}} = 10^{46}$ erg s$^{-1}$) and thus the QSO phase does not appear. This is because the BH growth is greatly suppressed (see the bottom panel in Figure 9 and discussion in Section 3.2). Thus, the Eddington-limited growth model for $z_i = 8$ cannot explain the observed distant luminous QSOs. Also, the nuclear starburst activity dominates the AGN activity, and the peak nuclear starburst luminosity is $\sim 10^{43}$ erg s$^{-1}$. Such an intense starburst would be observed in the infrared band because of the strong dust extinction. If this is the case, we may discover a hyper-luminous infrared galaxy without a bright AGN at $z \sim 7$. Moreover, we predict a strong AGN outflow with $M_{\text{outflow}} \approx 10^7 M_\odot$ yr$^{-1}$ in the nuclear starburst dominated phase (bottom panel in Figure 9). Here the total outflow mass is obtained by $M_{\text{outflow}} \equiv \int_0^t M_{\text{outflow}}(t') dt'$. Figure 10 (top panel) shows that the peak AGN luminosity is comparable to $L_{QSO, \text{th}}$ for the Eddington-limited growth model for $z_i = 25$. This is because the final BH mass is comparable to that for the super-Eddington growth model (see Figure 1 and the discussion in Section 3.2). Thus, this model can marginally reproduce the observable properties of QSOs at $z \sim 6$. However, it is hard to form more luminous distant QSOs at $z > 8$ by the
Eddington-limited growth as far as the radiative efficiency is $\epsilon_{\text{BH}} \sim 0.1$. Thus, it is essential to discover the distant luminous QSOs by the future deep wide-field survey. Figure 10 (top panel) also shows that the nuclear-starburst luminosity dominates the AGN luminosity in the proto-QSO phase (i.e., $L_{\text{SB}} \gg L_{\text{AGN}}$). This is different from the results of the super-Eddington growth model. On the other hand, the evolution of $M_{\text{g}}(t)$ and $M_{\text{e}}(t)$ are the same as the results of super-Eddington growth model (see Figure 8(a)). Thus, it is predicted that a stellar rich massive CND exists in the QSO phase and for the proto-QSO phase there exists a gas-rich massive CND (see the bottom panel in Figure 10).

5. APPLICATION TO THE DISTANT QSO SDSS J1148+5251 AT $z = 6.42$

We here compare our predictions (Section 4) with a distant QSO, the well known and examined SDSS J1148+5251 at $z = 6.42$. We summarize the properties of this QSO elucidated by using multi-wavelengths. The bolometric QSO luminosity is $L_{\text{AGN}} \sim 10^{47}$ erg s$^{-1}$ by near infrared observations (e.g., Wilcott et al. 2003; Barth et al. 2003). The radio and submillimeter observations suggest vigorous star formation in $\sim$ kpc with $\sim 10^2 M_\odot$ yr$^{-1}$ (Bertoldi et al. 2003b; Carilli et al. 2004; Walter et al. 2009). In addition, the molecular gas in the central $\sim 6$ kpc is $\sim 5 \times 10^{10} M_\odot$ by using carbon monoxide (CO) emission (Walter et al. 2003, 2004; Bertoldi et al. 2003a). However, we should note that the observed emission line might be sitting on top of a much broader line, because the low signal-to-noise ratio of the current data is not enough to determine the emission with accuracy (Narayanan et al. 2008).

The observed high luminosity with $L_{\text{AGN}} \sim 10^{47}$ erg s$^{-1}$ could correspond to the late growth of SMBH with $z_i = 8$ (see Figure 7(b)) rather than the early growth of SMBHs with $z_i = 25$ (see Figure 7(a) and Figure 10 (top panel)). If this is the case, the rapid and high mass accretion from $\sim$ kpc scale (i.e., $M_{\sup} \approx 10^3 M_\odot$ yr$^{-1}$ and $M_{\sup} \approx 10^{11} M_\odot$) is required. Thus, the presence of massive CNDs with $M_{\text{g}} = 5 \times 10^{10} M_\odot$ and a luminous nuclear starburst in the infrared band with $L_{\text{SB}} \approx 10^{47}$ erg s$^{-1}$ is predicted. These values are larger than the case of the early growth of SMBHs with $z_i = 25$, i.e., $M_{\text{g}} < 10^{10} M_\odot$ and $L_{\text{SB}} \approx 2 \times 10^{46}$ erg s$^{-1}$. The predicted CNDs can be observed through CO and hydrogen cyanide molecular emission using ALMA even at $z \sim 6$ because of $M_{\text{g}} \approx 10^{10}$--$10^{11} M_\odot$ in the CND (e.g., Kawakatu et al. 2006). The PAH emission is a powerful indicator of the obscured starburst activity (e.g., Imanishi 2002). For $3.3 \mu$m (the rest frame) PAH emission from CNDs at $z = 6$, $\sim 3 \times 10^{-19}$ W m$^{-2}$ line flux is expected at $\sim 25 \mu$m at the observed frame, assuming that the ratio of $3.3 \mu$m PAH emission and the total infrared luminosity is $\approx 10^{-3}$ for pure starburst galaxies (e.g., Mouri et al. 1990; Imanishi 2002). The Space Infrared Telescope for Cosmology and Astrophysics (SPICA) and the James Webb Space Telescope (JWST) through polycyclic aromatic hydrocarbon (PAH) emission could also detect dusty starbursts in CNDs of this QSOs because the predicted value is above the line sensitivity limit (Swinyard et al. 2009). The present model can be verified by these future observations.

On the basis of the present results, we will constrain the host mass of the $z = 6.42$ QSO SDSS J1148+5251. The mass accretion due to the tidal torque driven by the major and minor merger of galaxies is an essential process during the hierarchical formation of galaxies (e.g., Toomre & Toomre 1972; Mihos & Hernquist 1994, 1996; Saitoh & Wada 2004; Saitoh et al. 2008). Saitoh & Wada (2004) examined the evolution of stellar and gaseous cores on a sub-kpc scale during the formation of a spiral galaxy by hierarchical mergers, and found that the galactic core ($< 300$ pc) coevolves with the galactic DM halo of $\sim 10$ kpc scale. The average mass ratio between the gas component in the core, $M_{\text{core}}$, and the DM halo, $M_{\text{DM}}$ is nearly constant, $M_{\text{core}}/M_{\text{DM}} \sim 0.04$. If we assume that the galactic core corresponds to the CNDs, i.e., $M_{\text{core}} = M_{\sup}$, QSOs at $z > 6$ would be formed in a massive DM halo of $M_{\text{DM}} > 10^{12} M_\odot$ because of $M_{\sup} > 10^{10} M_\odot$. A massive halo of $\sim 10^{12}$--$10^{13} M_\odot$ was also suggested by Li et al. (2007) to explain the low space density of bright QSOs at $z \sim 6$ (e.g., Fan et al. 2001). Alternatively, Umemura (2001; hereafter U01) proposed another mass accretion process, i.e., the mass accretion onto the galactic center from a galactic scale ($\sim$kpc) via the radiation drag (see also Kawakatu & Umemura 2002). According to U01, the maximal mass accretion rate in the optically thick regime is given by $M_{\text{drag}} = L_{\text{host}}/c^2 \approx 0.1 M_\odot$ yr$^{-1}$($L_{\text{host}}/10^{42}$ $L_\odot$), where $L_{\text{host}}$ is the luminosity of host galaxies. To reproduce the rapid mass infall, e.g., $M_{\sup} \approx 10 M_\odot$ yr$^{-1}$, the hosts of proto-QSOs must have strong star formation with $L_{\text{host}} \approx$
10^{14} L_\odot. If this is the case, the stellar mass of the QSO host can be $M_{\text{host}} \approx 10^{13} M_\odot$ because of $M_{\text{BH}} \approx 0.001 M_{\text{host}}$ (U01; Kawakatu et al. 2003). These discussions indicate that the SDSS J1148+5251 form in massive DM halos and/or massive hosts (i.e., $M_{\text{DM}} \approx 10^{12}-13 M_\odot$ and/or $M_{\text{host}} \approx 10^{13} M_\odot$), in order to build a SMBH with $> 10^9 M_\odot$ only by the gas accretion. This point should be tested by the future deep wide-field AGN survey.

Moreover, we discuss the nature of the progenitor of SDSS J1148+5251. As seen in Figure 7(b), the AGN luminosity is still bright with $L_{\text{AGN}} \approx 10^{49}$ erg s$^{-1}$ at $z \sim 7.5$. It is hard to observe the AGN feature in the optical and X-ray observations because the AGN could be obscured by the dusty CND and dusty hosts (see Figure 6). We predict that the progenitor can be super-Eddington objects (see Figure 7(b)) and observed as high-$z$ ULIRGs such as SMGs with $L_{\text{IR}} \approx 10^{10}$ erg s$^{-1}$ because of $L_{\text{AGN}} \approx L_{\text{SB}}$. It is also predicted that the progenitor has a gas-rich CND with the mass ratio $M_{\text{g}}/M_{\text{dyn}} \approx 1$. Such a gas-rich CND with $M_{\text{g}} \sim 10^{10-11} M_\odot$ can be detected by ALMA.

6. SUMMARY

Based on the physical model of SMBH growth via gas accretion in $\sim 100$ pc scale CNDs proposed by Kawakatu & Wada (2008), we investigate the formation of high-$z$ ($z > 6$) QSOs whose BH masses are $M_{\text{BH}} > 10^9 M_\odot$. We show the necessary conditions to form QSOs at $z > 6$, in terms of the total gas mass accreted from host galaxies, $M_{\text{sup}}$ and star formation efficiency in the CND, $C_\ast = M_\ast/M_g$ where $M_\ast$ and $M_g$ are the star formation rate and the gas mass, respectively. Our main conclusions are summarized as follows.

1. The required conditions for the formation of QSOs at $z > 6$ are as follows. (1) Rapid and large mass supply with $M_{\text{sup}} > 10^{10} M_\odot$ within 1 Gyr from hosts to CNDs, because the final BH mass is only 1%--10% of the total mass supplied from hosts. The fraction is determined by the efficiency with which SN energy is transferred to the cold gas, and the efficiency of angular momentum transfer due to turbulent viscosity. (2) High star formation efficiency, i.e., $10^{-8}$ yr$^{-1} < C_\ast < 10^{-6}$ yr$^{-1}$ is comparable to high-$z$ starburst galaxies such as SMGs. (3) Rapid mass inflow from hosts with a period of the mass supply, $t_{\text{sup}} < 5 \times 10^9$ yr.

2. We find that if the BH growth is limited by the Eddington accretion, the final BH mass is greatly suppressed when the period of mass supply from hosts, $t_{\text{sup}}$, is shorter than the Eddington timescale. Thus, the super-Eddington growth is required for the QSO formation, while $t_{\text{sup}}$, which is determined by the efficiency of angular momentum transfer, is shorter than $\sim 10^9$ yr.

3. On the basis of these results, we predict the observable properties and the evolution of QSOs at $z > 6$ as follows. (1) The evolution of the QSO luminosity strongly depends on the redshift $z_i$ at which the accretion onto a seed BH got started. In other words, the bright QSOs given $z \sim 6$ favors the late growth of SMBHs (i.e., $z_i \approx 10$) rather than the early growth (i.e., $z_i \approx 30$) because the timescale of gas supplied from hosts is shorter than that of the star formation in the CND. (2) In the QSO phase, after which the gas supply stopped and when the AGN luminosity is above the threshold one, $L_{\text{AGN,th}}$ (e.g., $L_{\text{AGN,th}} \approx 10^{46}$ erg s$^{-1}$), there exists a stellar rich massive CND with $M_{\text{g}}/M_{\text{dyn}} \approx 0.1$ where $M_{\text{dyn}}$ is the dynamical mass of the CND plus BH.

On the other hand, in the proto-QSO phase (the early phase of a growing BH), the proto-QSO has a gas-rich massive CNDs with $M_{\text{g}}/M_{\text{dyn}} \approx 1$.

4. Our theoretical model predicts that the distant QSO SDSS J1148+5251 discovered at $z = 6.42$ favors the model of late growth of SMBH with $z_i = 8$ rather than early growth with $z_i = 25$. If this is the case, the QSO harbors a massive CNDs with $M_{\text{g}} = 5 \times 10^{10} M_\odot$ and the luminous nuclear starburst in the infrared band with $L_{\text{SB}} \approx 10^{47}$ erg s$^{-1}$. These predictions can be checked by the future observations (e.g., ALMA, SPICA, and JWST), in order to judge whether our model is reasonable for the formation of SMBHs. In addition, we predict that SDSS J1148+5251 have been evolved in a massive DM halo and/or a massive host (i.e., $M_{\text{DM}} \approx 10^{12-13} M_\odot$ and/or $M_{\text{host}} \approx 10^{13} M_\odot$), in order to build a SMBH with $> 10^9 M_\odot$ only by gas accretion. The progenitor of SDSS J1148+5251 can be super-Eddington objects and observed as the high-$z$ ULIRGs such as SMGs with the infrared luminosity $L_{\text{IR}} \sim 10^{46}$ erg s$^{-1}$. The progenitor has a gas-rich CND with the mass ratio $M_{\text{g}}/M_{\text{dyn}} \approx 1$ and $M_{\text{g}} \geq 10^{5} M_\odot$, which will be observed by ALMA.

We appreciate many valuable suggestions and comments of anonymous referees. We thank A. Ferrara, F. Takahara and M. Umemura for useful comments and discussions. We thank T. Elizabeth for carefully reading the manuscript. N.K. is financially supported by the Japan Society for the Promotion of Science (JSPS) through the JSPS Research Fellowship for Young Scientists.

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