apk2vec: Semi-supervised multi-view representation learning for profiling Android applications

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ABSTRACT

Building behavior profiles of Android applications (apps) with holistic, rich and multi-view information (e.g., incorporating several semantic views of an app such as API sequences, system calls, etc.) would help catering downstream analytics tasks such as app categorization, recommendation and malware analysis significantly better. Towards this goal, we design a semi-supervised Representation Learning (RL) framework named apk2vec to automatically generate a compact representation (aka profile/embedding) for a given app. More specifically, apk2vec has the three following unique characteristics which make it an excellent choice for large-scale app profiling: (i) it encompasses information from multiple semantic views such as API sequences, permissions, etc., (ii) being a semi-supervised embedding technique, it can make use of labels associated with apps (e.g., malware family or app category labels) to build high quality app profiles, and (iii) it combines RL and feature hashing which allows it to efficiently build profiles of apps that stream over time (i.e., online learning).

The resulting semi-supervised multi-view hash embeddings of apps could then be used for a wide variety of downstream tasks such as the ones mentioned above. Our extensive evaluations with more than 42,000 apps demonstrate that apk2vec’s app profiles could significantly outperform state-of-the-art techniques in four app analytics tasks namely, malware detection, familial clustering, app clone detection and app recommendation.

KEYWORDS

Representation Learning, Graph Embedding, Skipgram, Malware Detection, App Recommendation

1 INTRODUCTION

The low threshold for entering the official and third-party Android app markets has attracted a large number of developers, resulting in an exponential growth of apps. At the point of this writing, Google play [1] is hosting more than 3.6 million apps [2], with thousands of new apps being added daily. Due to the wide range of functionalities provided by the apps (e.g., online shopping, banking, etc.), they have become an indispensable part of people’s daily life. However, this astronomical volume of functionality rich apps, has raised several challenging issues. A few significant ones are as follows: (i) app markets are facing difficulties in organizing large volumes of diverse apps to allow convenient and systematic browsing by the users, (ii) due to the rapid growth rate in app volumes, it is becoming increasingly tough for markets to recommend up-to-date and meaningful apps that matches users’ search queries, and (iii) with a significant number of plagiarists and malware authors hidden among app developers, these markets have been plagued with app clones and malicious apps.

One could observe that a systematic and deep understanding of apps’ behaviors is essential to solve the aforementioned issues. Building high-quality behavior profiles of apps could help in determining the semantic similarity among the apps, which is pivotal to addressing these issues. Recent research [23, 24, 29, 32–38] reveals that compared to primitive representations of programs (e.g., counts of system-calls, Application Programming Interfaces (APIs) used etc.) graph representations (e.g., Control Flow Graphs (CFGs), call graphs, etc.) are ideally suited for app profiling, as the latter retain program semantics well, even when the apps are obfuscated. Reinforcing this fact, many recent works achieved excellent results using graph representations along with Machine Learning (ML) techniques on a plethora of program analytics tasks such as malware detection [23, 24, 32, 33, 38], familial classification [37], clone detection [29, 42], library detection [39] etc. In effect, these works cast their respective program analytics task as a graph analytics task and apply existing graph mining techniques [33] to solve them. Typically, these ML algorithms work on vectorial representations (aka embeddings) of graphs. Hence, arguably, one of the most important factors that determines the efficacy of these downstream analytics tasks is the quality of such embeddings.

Besides the choice of graph representations, another pivotal factor that influences the aforementioned tasks are the features that could be extracted from them. In the case of app analytics, the most prominent features in recent literature include API/system-call sequences observed [23], permissions [27] and information source/sinks used [31], etc. Evidently, each of these feature sets provides a different semantic perspective (interchangeably referred as view) of the apps’ behavior with different inherent strengths and limitations. As revealed by existing works [24, 27], capturing multiple semantic views with different modalities would help to improve the accuracy of downstream tasks significantly. Furthermore, any form of labeling information (e.g., malware family label, app category label, etc.) could be of significant help in building semantically richer and more accurate app profiles.

Towards catering the above-mentioned applications, in this work, we propose a Representation Learning (RL) technique to build data-driven, compact and versatile behavior profiles of apps. Based on the above observations, the following challenges have to be addressed to obtain such a profile:

(C1) Handcrafted features. Graph representations of programs such as CFGs are highly expressive data structures. Consequently,
representing them as vectors without losing much of their expressiveness is non-trivial. A typical solution is to use graph kernels [19, 20, 40, 41] which leverage on graph substructures (e.g., shortest paths, graphlets etc.) to build graph embeddings. However, these substructures are *handcrafted*. Therefore, when used on large datasets, these features lead to building high dimensional, sparse and non-smooth graph embeddings which do not generalize well and thus yield suboptimal accuracies [10, 11].

**(C2) Fully supervised or unsupervised RL.** Addressing the limitations of graph kernels, several data-driven supervised (e.g., CNNs [16], RNNs [17]) and unsupervised (e.g., skipgrams [9, 25], autoencoders [18]) graph embedding approaches have been proposed. Both types of approaches exhibit good generalization and offer excellent accuracies. However, the supervised embedding methods suffer from the following limitations: (i) they require typically large volumes of labeled graphs to learn meaningful embeddings, which is undesirable and often impractical for large-scale app analytic tasks, and (ii) the embeddings thus learnt are specific to one particular analytics task and may not be transferable to others. On the other hand, unsupervised embedding methods do not exhibit these limitations. However, in many cases, a portion of the dataset may have labels or some samples may have more than one label (e.g., an app may have several labels such as category to which it belongs, whether or not it is malicious, etc.). Unsupervised embedding approaches are incapable of leveraging such labels which contain valuable semantic information.

**(C3) Scalability.** Though RL based methods provide graph embeddings which generalize well, when used on large datasets, they exhibit poor scalability both in terms of memory and time requirements. This is because they have extremely large number of parameters to train (especially in models such as RNNs and skipgrams).

**(C4) Integrating information from multiple views.** All the above mentioned approaches are typically designed to capture only one semantic view of the program through their embeddings. This severely limits their potentials to cater to a wide range of downstream tasks. Effectively integrating information from multiple views is challenging, but of paramount importance in building comprehensive embeddings capable of catering to a variety of tasks.

**Our approach.** Driven by these motivations, we develop a static analysis based semi-supervised multi-view RL framework named apk2vec to build high-quality data-driven profiles of Android apps. apk2vec has two major phases: (1) a *static analysis phase* in which a given app file is disassembled and three different dependency graphs (DGs), each representing a distinct semantic view are extracted and, (2) an *embedding phase* in which a neural network is used to combine the information from these three DGs and label information (if available) to learn one succinct embedding for the app. To this end, apk2vec combined and extends several state-of-the-art RL ideas such as multimodal (aka multi-view) RL, semi-supervised neural embedding and feature hashing.

apk2vec addresses the above-mentioned challenges in the following ways:

- **Data-driven embedding:** Unlike graph kernels, apk2vec uses a skipgram neural network [4, 25] that automatically learns features from large corpus of graph data to produce high quality dense embeddings. This in effect addresses challenge C1.
- **Semi-supervised task-agnostic embedding:** apk2vec’s neural network facilitates using class labels of apks (incl. multiple labels per sample) if they are available to build better app profiles. However, these embeddings are still task-agnostics and hence can be used for a variety of downstream tasks. This helps addressing challenge C2.
- **Hash embedding:** Recently, Svenstrup et al [5] proposed a scalable feature hashing based word embedding model which required much lesser number of trainable parameters than conventional RL models. Besides this improvement in efficiency, hash embedding model also facilitates learning embeddings when instances stream over time. Inspired by this idea, in apk2vec, we develop an efficient hash embedding model for graph/subgraph embedding, thus addressing challenge C3.
- **Multi-view embedding:** apk2vec’s neural network facilitates multimodal RL through a novel learning strategy (see §4.3). This helps to integrate three different DGs that emerge from a given app file and produce one common embedding. Thus apk2vec facilitates combining information from different views in a systematic and non-linear manner, thereby addressing challenge C4.

**Experiments.** To evaluate our approach, we perform a series of experiments on various app analytics tasks (incl. supervised, semi-supervised and unsupervised learning tasks), using a dataset of more than 42,000 real-world Android apps. The results show that our semi-supervised multimodal embeddings can achieve significant improvements in terms of accuracies over unsupervised/unimodal RL approaches and graph kernel methods while maintaining comparable efficiency. The improvements in prediction accuracies range from 1.74% to 5.93% (see §5 for details).

In summary, we make the following contributions:

- We propose apk2vec, a static analysis based data-driven semi-supervised multi-view graph embedding framework, to build task-agnostic profiles for Android apps (§4). To the best of our knowledge, this is the first app profiling framework that has three aforementioned unique characteristics.
- We propose a novel variant of the skipgram model by introducing a view-specific negative sampling technique which facilitates integrating information from different views in a non-linear manner to obtain multi-view embeddings (§4.7).
- We extend the feature hashing based word embedding model to learn multi-view graph/subgraph embeddings. Hash embeddings improve apk2vec’s overall efficiency and support online RL (§4.6).
- We make an efficient implementation of apk2vec and the profiles of all the apps used in this work publicly available at [22].

2 PROBLEM STATEMENT

Given a set of *apks* \( A = \{a_1, a_2, \ldots, a_n\} \), a set of corresponding labels \( \mathbb{L} = \{l_1, l_2, \ldots\} \) (some of which may be empty i.e., \( \forall l_i \in \mathbb{L}, |l_i| \geq 0 \)) for each app in \( A \) and a positive integer \( \delta \) (i.e., embedding size), we intend to learn \( \delta \)-dimensional distributed representations for every *apk* \( a_i \in A \). The matrix representations of all *apks* is denoted as \( \Phi^A \in \mathbb{R}^{|A| \times \delta} \).
More specifically, \( a_i \in A \) can be represented as a three-tuple: 
\[ a_i = (G^i_U, \lambda^i_U, \lambda^i_L) \]
where \( u \in \{ A, P, S \} \) and \( G^A_U, G^P_U, G^S_U \) denote its API Dependency Graph (ADG), Permission Dependency Graph (PDG), and information Source & Sink Dependency Graph (SDG), respectively (refer to §4.2 for details on constructing these DGs). Furthermore, a DG can be represented as \( G^i_U = (N^i_U, E^i_U, \lambda^i_U) \), where \( N^i_U \) is the set of nodes and \( E^i_U \subset N^i_U \times N^i_U \) is the set of edges in \( G^i_U \). A labeling function \( \lambda^i_U : N^i_U \rightarrow \lambda^i_U \) assigns a label to every node in \( N^i_U \) from alphabet set \( \lambda^i_U \).

Given \( G^i_U = (N^i_U, E^i_U, \lambda^i_U) \) and \( s^g = (N^g_U, E^g_U, \lambda^g_U) \), \( g^s \) is a subgraph of \( G \) iff there exists an injective mapping \( \mu : N^g_U \rightarrow N^U \) such that \((n_1, n_2) \in E^g_U \iff (\mu(n_1), \mu(n_2)) \in E^U \). In this work, by subgraph, we strictly refer to a specific class of subgraphs, namely, rooted subgraphs. In a given graph \( G^i_U \), a rooted subgraph of degree \( d \) around node \( n \in N^G_U \) encompasses all the nodes (and corresponding edges) that are reachable in \( d \) hops from \( n \).

3 BACKGROUND & RELATED WORK

Our goal is to build compact multi-view behavior profiles of apk files in a scalable manner. To this end, we develop a novel apk embedding framework by combining several RL ideas such as word, document and graph embedding models and feature hashing. Hence, in this section, the related background from these areas are reviewed.

3.1 Skipgram word and document embedding model

The popular word embedding model word2vec[4] produces word embeddings that capture meaningful syntactic and semantic regularities. To learn word embeddings, word2vec uses a simple feed-forward neural network architecture called skipgram. It exploits the notion of context such that, given a sequence of words \( \{w_1, w_2, ..., w_T\} \), the target word \( w_t \) whose representation has to be learnt and the length of the context window \( c \), the objective of skipgram model is to maximize the following log-likelihood:

\[
\sum_{t=1}^{T} \log \Pr(w_{t-c}, ..., w_{t+c} | w_t) = \sum_{t=1}^{T} \log \prod_{c \leq j \leq c} \Pr(w_{t+j} | w_t) \]  \( (1) \)

where \( w_{t-c}, ..., w_{t+c} \) are the context words and \( \mathcal{H} \) is the vocabulary of all the words. Here, the context and target words are assumed to be independent. Furthermore, the term \( \Pr(w_{t+j} | w_t) \) is defined as:

\[
\frac{e^{\langle \mathbf{w}_j, \mathbf{w}_t \rangle}}{\sum_{w \in \mathcal{H}} e^{\langle \mathbf{w}_j, \mathbf{w} \rangle}}
\]

where \( \mathbf{w} \) and \( \mathbf{w}_j \) are the input and output embeddings of word \( w \), respectively. In the face of very large \( \mathcal{H} \), the posterior probability in eq.\((1)\) could be learnt in an efficient manner using the so-called negative sampling technique.

**Negative Sampling.** In each iteration, instead of considering all words in \( \mathcal{H} \) a small subset of words that do not appear in the target word’s context are selected at random to update their embeddings. Training this way ensures the following: if a word \( w_t \) appears in the context of another word \( w_j \), then the embedding of \( w_t \) is closer to that of \( w_j \) compared to any other randomly chosen word from \( \mathcal{H} \).

Once skipgram training converges, semantically similar words are mapped to closer positions in the embedding space revealing that the learnt embeddings preserve semantics.

Le and Mikolov’s doc2vec[6] extends the skipgram model in a straightforward manner to learn representations of arbitrary length word sequences such as sentences, paragraphs and whole documents. Given a set of documents \( D = \{d_1, d_2, ...\} \) and a set of words \( c(d_t) = \{w_1, w_2, ...\} \) sampled from document \( d_t \in D \), doc2vec skipgram learns a \( \delta \) dimensional embeddings of the document \( d_t \) and each word \( w_t \in c(d_t) \). The model works by considering a word \( w_t \in c(d_t) \) to be occurring in the context of document \( d_t \) and tries to maximize the following log likelihood:

\[
\sum_{j=1}^{T} \log \Pr(w_j | d_t)
\]

where the probability \( \Pr(w_j | d_t) \) is defined as:

\[
\frac{e^{\langle \mathbf{w}_j, \mathbf{w} \rangle}}{\sum_{w \in \mathcal{W}} e^{\langle \mathbf{w}_j, \mathbf{w} \rangle}}
\]

Here, \( \mathcal{T} \) is the vocabulary of all the words across all documents in \( D \). Understandably, doc2vec skipgram could be trained efficiently using negative sampling.

**Model parameters.** From the explanations above, it is evident that the total number of trainable parameters of skipgram word and document embedding skipgram models would be \( 2|\mathcal{T}| \delta + \delta (|D| + |\mathcal{T}|) \), respectively.

3.2 Hash embedding model

Though skipgram emerged as a hugely successful embedding model, it poses scalability issues when the vocabulary \( \mathcal{T} \) is very large. Also, its architecture does not support learning embeddings when new words (aka new tokens) stream over time. To address these issues, Svenstrup et al. [5] proposed a feature hashing based word embedding model. This model involves the following steps:

1. A token to id mapping function, \( \mathcal{F} : \mathcal{T} \rightarrow \{1, ..., K\} \) and \( k \) hash functions of the form \( \mathcal{H}_i : \{1, ..., K\} \rightarrow \{1, ..., B\}, i \in \{1, k\} \) are defined (\( B \) is the number of hash buckets and \( B << K \)).
2. The following arrays are initialized: \( \Phi(b) \rightarrow \{ \} \) a pool of \( B \) component vectors which are intended to be shared by all words in \( \mathcal{T} \), and \( \Phi(K) \rightarrow \{ \} \) contains the importance of each component vector for each word.
3. Given a word \( w \in \mathcal{T} \), hash functions \( \mathcal{H}_1, ..., \mathcal{H}_K \) are used to choose \( k \) component vectors from the shared pool \( \Phi \).
4. The component vectors from step (3) are combined as a weighted sum to obtain the hash embedding of the word \( w \):
   \[ w = \sum_{i=1}^{K} \mathbf{w}_i \mathcal{H}_i(w) \]
5. With hash embeddings of target and context words thus obtained, skipgram model could be used to train for eq.\((1)\). However, unlike regular skipgram which considers \( \Phi \) alone as a set of trainable parameters, one could train \( p \) as well.

Thus Svenstrup et al’s framework reduces the number of trainable parameters from \( 2K\delta \) to \( 2(B\delta + K \delta) \), which helps reducing the pretraining time and memory requirements. The effect of collisions from \( K \) to \( B \) could be minimized by having more than one hash function and this helps in maintaining accuracies on-par with word2vec. Besides, when new words arrive over time, a function like MD5 or SHA1 could be used in place of \( \mathcal{F} \) to hash them to a fixed set of integers in range \([1, K]\). This helps learning word embeddings in an online fashion.

3.3 Graph embedding models

Analogously, graph2vec[25] considers simple node labeled graphs such as CFGs as documents and the rooted subgraphs around every node in them as words that compose the document. The intuition
is that different subgraphs compose graphs in a similar way that
different words compose documents. In this way, graph2vec could
be perceived as an RL variant of Weisfeiler-Lehman kernel (WLK)
which counts the number of common rooted subgraphs across a
pair of graphs to estimate their similarity. As such, graph2vec is
capable of learning embeddings of arbitrary sized graphs.

Given a dataset of graphs \( \mathcal{G} = \{G_1, G_2, \ldots \} \), graph2vec extends
the skipgram model explained in §3.1 to learn embeddings of each
graph. Let \( G_i \in \mathcal{G} \) be denoted as \((N_i, E_i, \lambda)\) and the set of all rooted
subgraphs around every node \( n \in N_i \) (up to a certain degree \( D \)) be
denoted as \( \mathcal{c}(G_i) \). graph2vec aims to learn a \( \delta \) dimensional embed-
dings of the graph \( G_i \) and each subgraph \( s \in \mathcal{c}(G_i) \) sampled from \( \mathcal{c}(G_i) \)
\( \mathcal{G}_i, s \in \mathbb{R}^\delta \), respectively by maximizing the following log like-
lihood: \( \sum_{j=1}^{\mathcal{c}(G_i)} \log \Pr(s_j|G_i) \), where the probability \( \Pr(s_j|G_i) \)
is defined as:

\[
\frac{e^{\mathcal{G}_i(s_j)}}{\sum_{s \in T} e^{\mathcal{G}_i(s)}}
\]

Here, \( T \) is the vocabulary of all the sub-
graphs across all graphs in \( \mathcal{G} \). The number of trainable parameters
of this model will be \( \delta(|G| + |T|) \).

Similar to graph2vec, many recent approaches such as sub2vec [9], GE-FSG [45] and Anonymous Walk Embeddings (AWE) [46]
have adopted skipgram architecture to learn unsupervised graph
embeddings. The fundamental difference among them is the type
of graph substructure that they consider as a graph’s context. For
instance, sub2vec considers nodes, GE-FSG considers frequent sub-
graphs (FSGs) and AWE considers walks that exist in graphs as
their contexts, respectively.

### 3.4 Semi-supervised embedding model

Recently, Pan et al. [14] extended the skipgram model to learn embed-
ing of nodes in Heterogeneous Information Networks (HINs)
in a semi-supervised fashion. Specifically, their extension facilitates
skipgram to use class labels of (a subset of) samples while building
embeddings. For instance, when \( l_i \), the class label of a document \( d_i \)
is available, the doc2vec model could maximize the following log
likelihood:

\[
\beta \sum_{j=1}^{\mathcal{c}(d_i)} \log \Pr(w_j|d_i) + (1 - \beta) \sum_{j=1}^{\mathcal{c}(d_i)} \log \Pr(w_j|l_i)
\]

to include the supervision signal available from \( l_i \) along with the
contents of the document made available through \( c(d_i) \). Here, \( \beta \) is
the weight that balances the importance of the two components
in document embedding. Pan et al. empirically prove that embed-
dings with this form of semi-supervision significantly improves the
accuracy of downstream tasks.

In summary, all above-mentioned embedding models possess
some strengths for RL in various areas mainly for natural lan-
guage texts. Differing from them, we propose a new and efficient
data-driven graph embedding model/framework for app behaviour
profiling. The new framework has three unique characteristics
which brings in crucial strengths for holistic app behaviour profiling,
namely: (i) multi-view RL, (ii) semi-supervised RL, and (iii) feature
hashing based RL. We illustrate (both in principle and through ex-
periments) that this new framework possess all these strengths and
caters a multitude of downstream tasks.

### 4 METHODOLOGY

In this section, we explain the apk2vec app profiling framework.
We first present an overview of the framework which encompasses
two phases, subsequently, we discuss the details of each component
in the following subsections.

#### 4.1 Framework Overview

As depicted in Figure 1, the workflow of apk2vec can be divided
into two major phases, namely, the static analysis phase and the
embedding phase. The static analysis phase en masse of only
program analysis procedures which intend to transform apk files
into DGs. The subsequent embedding phase en masse RL tech-
niques that transform these DGs into apk profiles.

**Static analysis phase.** This phase begins with disassembling
the apks in the given dataset and constructing their interprocedural
CFG (ICFG). Further static analysis is performed to abstract each
ICFG into three different DGs, namely, ADG, PDG and SDG. Each
of them represent a unique semantic view of the app’s behaviors
with distinct modalities. Detailed procedure of constructing these
DGs is presented in §4.2.

![APK2VEC: Framework overview](image1)

![Semi-supervised Multi-view Skipgram](image2)
Embedding phase. After obtaining the DGs for all the apks in the dataset, rooted subgraphs around every node in the DGs are extracted to facilitate the learning apk embeddings. Once the rooted subgraphs are extracted, we train the semi-supervised multi-view skipgram neural network with them. The detailed procedure is explained in §4.3.

4.2 Static Analysis Phase

ICFG construction. Given an apk file, the first step is to perform static control-flow analysis and construct the ICFG. We chose ICFG over other program representation graphs (e.g., DFGs, call graphs) due to its fine-grained representation of control flow sequence, which allows us to capture finer semantic details of the apk which is necessary to build a comprehensive ICFG and one exit point which represents the largest piece of the program that is always the network intends to predict the API, permission and source-sink multi-view RL. More precisely, given an each view). The goal of the first input layer (ΦΔ) is to perform static control-flow analysis and construct its ICFG. We chose ICFG over other program representation graphs (e.g., DFGs, call graphs) due to its fine-grained representation of control flow sequence, which allows us to capture finer semantic details of the apk which is necessary to build a comprehensive apk profile. Formally, ICFG = (N, E) for an apk a is a directed graph where each node bb N denotes a basic block1 of a method m in a, and each edge e(bb1, bb2) ∈ E denotes either an intra-method control-flow or a calling relationship from bb1 to bb2 and E ⊆ N × N.

Abstraction into multiple views. Having constructed the ICFG, to obtain richer semantics from the apk, we abstract it with three Android platform specific analysis, namely API sequences, Android permissions, and information sources & sinks to construct the three DGs, respectively. The abstraction process is described below.

To obtain the ADG from a given ICFG, we remove all nodes that do not access security sensitive Android APIs. This will leave us with a subset of sensitive nodes from the perspective of API usages, say NΔ ⊆ N. Subsequently, we connect a pair of nodes n1, n2 ∈ NΔ iff there exist a path between them in ICFG. This yields the ADG, which could be formally represented as a three tuple GΔ = (NΔ, EΔ, λΔ), where λΔ : NΔ → LΔ is a labeling function that assigns a security sensitive API as a node label to every node in NΔ from a set of alphabets LΔ. We refer to existing work [23] for the list of security sensitive APIs. Similarly, we use works such as PScout [30] and SUSI [31] which maps APIs to Android permissions and information source/sinks to obtain set of node labels LP and LS, respectively. Subsequently, adopting the process mentioned above using them we abstract the ICFG into PDG and SDG using LP and LS, respectively.

4.3 Embedding Phase

In the embedding phase, our goal is to take the DGs and class labels that correspond to a set of apks and train the skipgram model to obtain the behavior profile for each apk. To this end, we develop a novel variant of the skipgram model which facilitates incorporating the three following learning paradigms: semi-supervised RL, multi-view RL and feature hashing.

Network architecture Figure 2 depicts the architecture of the neural network used in apk2vec’s RL process. The network consists of two shared input layers and three layered output layers (one for each view). The goal of the first input layer (ΦΔ) is to perform multi-view RL. More precisely, given an apk id ai in the first layer, the network intends to predict the API, permission and source-sink subgraphs that appear in ai’s context, in each of the output layers. Similarly, the goal of the second input layer (ΦΔ) is to perform semi-supervised RL. More specifically, given ai’s class label as input in the second layer, the network intends to predict subgraphs of all three views that occur in ai’s context in each of the output layers. Thus, the network forces API, permission and source-sink subgraphs that frequently co-occur with same class labels to have similar embeddings. For instance, given a malware family label f, subgraphs that characterize f’s behaviors would end up having similar embeddings. This in turn would influence apks that belong to f to have similar embeddings.

Hash embeddings. Considering the real-world scenario where Android platform evolves (i.e., APIs/permissions being added or removed) and apps stream rapidly over time, it is obvious that the vocabulary of subgraphs (across all DGs) would grow as well. Regular skipgram models could not handle such a vocabulary and as mentioned in §3.2, hash embeddings could be used effectively to address this. Note that in our framework, the vocabulary of tokens is only present in the output layer. Hence, in apk2vec, hash embeddings are used only in the three output layers (ΦΔ, ΦΔ and ΦΔ) and the two input layers (ΦΔ and ΦΔ) uses regular embeddings.

The process through with our skipgram model is trained is explained through Algorithm 1.

4.4 Algorithm: apk2vec

The algorithm takes the set of apks along with their corresponding DGs (A), set of their labels (L), maximum degree of rooted

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1 A basic block is a sequence of instructions in a method with only one entry point and one exit point which represents the largest piece of the program that is always executed altogether.
subgraphs to be considered \((D)\), embedding size \((\delta)\), number of epochs \((E)\), number of hash buckets per view \((B^v)\), number of hash functions \((k)\) and learning rate \((\alpha)\) as inputs and outputs the \(apk\) embeddings \((\Phi^\delta)\). The major steps of the algorithm are as follows:

1. We begin by randomly initializing the parameters of the model i.e., \(\Phi^\delta\): \(apk\) embeddings, \(\Phi^\delta\): label embeddings, \(\delta^v_i\): embeddings of each hash bucket for each of the three views, and \(p^v_i\): importance parameters for each of the views (line 1). It is noted that except the \(apk\) embeddings, all other parameters are discarded when training culminates.

2. For each epoch, we consider each \(apk\) \(a_i\) as the target whose embedding has to be updated. To this end, each of its DG \(G_i^d\) is taken and all the rooted subgraphs upto degree \(D\) around every node are extracted from the same (line 4). The subgraph extraction process is explained in detail in §4.5.

3. The set of all such subgraphs \(sg_c\) is perceived as the context of \(a_i\). Once \(sg_c\) is obtained, we get their hash embeddings and compute the negative log likelihood of their similarity to the context components (lines 7-9). This step amounts to semi-supervised RL as all the nodes are processed, rooted subgraphs of degrees \([0, D]\) are collected in \(S\) which is returned finally (line 12).

4. We begin by randomly initializing the parameters of the model i.e., \(\Phi^\delta\): \(apk\) embeddings, \(\Phi^\delta\): label embeddings, \(\delta^v_i\): embeddings of each hash bucket for each of the three views, and \(p^v_i\): importance parameters for each of the views (line 1). It is noted that except the \(apk\) embeddings, all other parameters are discarded when training culminates.

4.5 Extracting context subgraphs

For a given \(apk\) \(a_i\) extracting rooted subgraphs around each node in each \(G_i^d\) and considering them as its context is a fundamental task in our approach. To extract these subgraphs, we follow the well-known Weisfeiler-Lehman relabeling process [19] which lays the basis for WLK [11, 19]. The subgraph extraction process is presented formally in Algorithm 2. The algorithm takes the graph \(G\) from which the subgraphs have to be extracted and maximum degree to be considered around root node \(D\) as inputs and returns the set of all rooted subgraphs in \(G, S\) (line 2). It begins by initializing \(S\) to an empty set (line 2). Then, we extract rooted subgraph of degree \(d\) around each node \(n\) in the graph. When \(d = 0\), no subgraph needs to be extracted and hence the label of node \(n\) is returned (line 6). For cases where \(d > 0\), we get all the (breadth-first) neighbours of \(n\) in \(N_n\) (line 8). Then for each neighbouring node, \(n'\), we get its degree \(d - 1\) subgraph and save the same in a multiset \(M_{n}^{(d)}\) (line 9). Subsequently, we get the degree \(d - 1\) subgraph around the root node \(n\) and concatenate the same with sorted list \(M_{n}^{(d)}\) to obtain the subgraph of degree \(d\) around node \(n\), which is denoted as \(sg_n^{(d)}\) (line 10). \(sg_n^{(d)}\) is then added to the set of all subgraphs (line 11). When all the nodes are processed, rooted subgraphs of degrees \([0, D]\) are collected in \(S\) which is returned finally (line 12).

4.6 Obtaining hash embeddings

Once context subgraphs are extracted, we proceed with obtaining their hash embeddings and training the same along the target \(apk\)’s embedding. Given a subgraph, the process of extracting its hash embedding involves four steps which are formally presented in Algorithm 3. Following is the explanation of this algorithm:

1. Given a subgraph \(sg\), we begin by mapping to an integer \(sg_{id}\) using a function \(F^v\) (line 2). When \(T^v\), the vocabulary of all the subgraphs in view \(v\) could be obtained ahead of training, a regular dictionary aka token-to-id function which maps each subgraph to a unique number in the range \([1, K^v]\) (where \(K^v = |T^v|\)) could be used as \(F^v\). In the online learning setting, such a dictionary could not be obtained. Hence, analogous to feature hashing [26], one could use a regular hash function such as MDS or SHA1 to hash the subgraph to an integer in the predetermined range \([1, K^v]\) (here, an arbitrarily large value of \(K^v\) is chosen to avoid collisions).

2. \(sg_{id}\) is then hashed using each of the \(k\) hash functions. Each function \(H_i, i \in [1, K]\) maps it to one of the \(B^v\) available hash buckets which in turn maps to one of the \(B^v\) component embeddings in \(\delta^v\). Thus we obtain \(k\) component embeddings for the given subgraph and save them in \(components\) (line 3). In other words, \(components\) contains \(k\) \(\delta\)-dimensional embeddings.

3. Similarly, using \(sg_{id}\), we then lookup the importance parameter for each hash function, \(p^v_i(sg_{id}), i \in [1, k]\), and save them in \(weights\) (line 4). In other words, \(weights\) contains \(k\) importance values.

4. Finally, the hash embedding of the subgraph is obtained by multiplying \(k\) \(\delta\)-dimensional component vectors with \(k\) corresponding importance values (line 5).
Once the hash embeddings of the context subgraphs are obtained using the above mentioned process, one could train them along with the target apk’s embedding using a learning algorithm such as Stochastic Gradient Decent (SGD).

4.7 View-specific negative sampling

Similar to other skipgram based embedding models such as graph2vec [25], we could efficiently minimize the negative log likelihood in lines 5 and 8 of Algorithm 1. That is, given an apk a and a subgraph sgv which is contained in view v, the regular negative sampling intends to maximize the similarity between their embeddings. Besides, it chooses n subgraphs as negative samples i.e., that do not occur in the context of a and minimizes the similarity of a and these negative samples. This could be formally presented as follows,

\[ \Pr(sgv|a) = \sigma(\tilde{a}^T \cdot \tilde{sgv}) \prod_{j=1}^{n} E_{sgj \sim Pr_n(T)}(\sigma(-\tilde{a}^T \cdot \tilde{sgj})) \] (3)

where, \( T = \bigcup_v T^v \) is union of vocabularies across all views and \( E \) is expectation of choosing a subgraph sgj from the smoothed distribution of subgraphs Prn across all the three views.

In simpler terms, eq. (3) moves \( \tilde{a} \) closer to \( \tilde{sgv} \) as it occurs in \( a \)’s context and also moves \( \tilde{a} \) farther away from \( \tilde{sgj} \) (which may not belong to view v) as it does not occur in \( a \)’s context.

However, in our multi-view embedding scenario, the distribution of subgraphs is not similar across all views. For instance, in our experiments reported in §5, the API view produces millions of subgraphs as negative samples i.e., \( \tilde{sgj} \) which belongs to view \( v \) or \( \tilde{sgv} \) as negative samples. This could be formally presented as follows,

\[ \Pr(sgv|a) = \sigma(\tilde{a}^T \cdot \tilde{sgv}) \prod_{j=1}^{n} E_{sgj \sim Pr_n(T^v)}(\sigma(-\tilde{a}^T \cdot \tilde{sgj})) \] (4)

In simpler terms, eq. (4) moves \( \tilde{a} \) closer to \( \tilde{sgv} \) as it occurs in \( a \)’s context and also moves \( \tilde{a} \) farther away from \( \tilde{sgj} \) (which also belongs to view v) as it does not occur its \( a \)’s context.

4.8 Model dynamics

The trainable parameters of our model are \( \Phi^A, \Phi^L, \Phi^V, \) and \( \rho^v \). Recall, \( \Phi^A \) and \( \Phi^L \) are regular embeddings as they are in the input layers and \( \Phi^v \)’s are hash embeddings. Also, the total number of tokens in the input and output layers would be \(|A|+|L|\) and \( \sum_v K^v \), respectively. Hashing (which is applicable only to \( \Phi^v \)) reduces the number of parameters in the output layer from \( \sum_v K^v \) to \( K^v k + kB^v \) where \( B^v \ll K^v \) (typically, we set \( k = [2, 4] \) and \( K^v > B^v \cdot 100 \)).

From the explanations above, the computational overhead of using hash embeddings instead of standard embeddings is in the embedding lookup step. More precisely, a multiplication of a 1 \( \times \) \( k \) matrix (obtained from \( \rho^v \)) with a \( k \times \delta \) matrix (obtained from \( \Phi^v \)) is required instead of a regular matrix lookup to get a 1 \( \times \) \( \delta \) subgraph embedding. When using small values of \( k \), the computational overhead is therefore negligible. In our experiments, hash embeddings are marginally slower to train than standard embeddings on datasets with small vocabularies.

5 EVALUATION

We evaluate the efficacy of apk2vec’s embeddings with several tasks involving various learning paradigms that include supervised learning (batch and online), unsupervised learning and link prediction. The evaluation is carried out on five different datasets involving a total of 42,542 Android apps. In this section, we first present the experimental design aspects, such as research questions addressed, datasets and tasks chosen pertaining to the evaluation. Subsequently, the results and relevant discussions are presented.

Research Questions. Through our evaluations, we intend to address the following questions:

- How accurate do apk2vec’s embeddings perform on various app analytics tasks and how do they compare to state-of-the-art approaches?
- Do multi-view profiles offer better accuracies than single-view profiles?
- Does semi-supervised RL help improving the accuracy of app profiles?
- How does apk2vec’s hyperparameters affect its accuracy and efficiency?

Evaluation setup. All the experiments were conducted on a server with 40 CPU cores (Intel Xeon(R) E5-2640 2.40GHz), 6 NVIDIA Tesla V100 GPU cards with 256 GB RAM running Ubuntu 16.04.

Comparative analysis. To provide a comprehensive evaluation, we compare our approach with four baseline approaches, namely, WLK [19], graph2vec [25], sub2vec[9] and GE-FSG [45]. Refer to §1 and §3 for brief explanations on the baselines. The following evaluation-specific details on baselines are noted: (i) Since all baselines are unimodal they are incapable of leveraging all the three DGs to yield one unified apk embedding. Hence, to ensure fair comparison, we merge all three DGs into one graph and feed them to these approaches. (ii) sub2vec has two variants, namely, sub2vec_N (which leverages only neighborhood information for graph embedding) and sub2vec_S (which leverages only structural information). Both these variants are included in our evaluations, and (iii) For all baselines except GE-FSG, open-source implementations provided by the authors are used. For GE-FSG, we reimplemented it by following the process described in their original work. Our reimplementation could be considered faithful as it reproduces the results reported in the original work.

Hyperparameter choices. In terms of apk2vec’s hyperparameters, we set the following values: \( E = 100, \delta = 64, \alpha = 0.1 \) (with decay) and \( \eta = 2 \). When hash embedding is used \( k = 2, B^v = \frac{K^v}{64} \) (for all \( v \)). To ensure fair comparison, in all experiments, the hyperparameters of all baseline approaches are maintained same as those of apk2vec (e.g., the embedding dimensions of all baselines are set to 64, etc.). In all experiments, for datasets where class labels are available, 25% of the labels are used for semi-supervision during embedding (unless otherwise specified).

5.1 apk2vec vs. state-of-the-art

In the following subsections we intend to evaluate apk2vec against the baselines on two classification (i.e., batch and online malware
Table 1: Datasets used for evaluations

| Task                   | Data source                      | # of apps | Avg. nodes       | Avg. edges       |
|------------------------|----------------------------------|-----------|------------------|------------------|
| Batch malware detection| Malware: [27]                    | 19,944    | 80.03            | 141.75           |
|                        | Benignware: [3]                  | 20,000    | 93.12            | 135.99           |
| Online malware detection| Malware: [27]                    | 5,560     | 63.15            | 37.85            |
|                        | Benignware: [3]                  | 5,000     | 74.49            | 66.96            |
| Malware familial clustering| Drebin [27]                  | 5,560     | 229.82           | 69.96            |
|                        | Clone apps [29]                  | 289       | 174.74           | 54.92            |
| Clone detection        | Googleplay [3]                   | 2,318     | 2168.88          | 242.87           |
| App recommendation     |                                  |           |                  |                  |

Table 2: Malware detection (graph classification) results

| Technique | Batch | Online |
|-----------|-------|--------|
|           | F1    | M1    | F1    | M1    |        | F1    | M1    |
| apk2vec   | 88.87 | 90.41 | 87.90 | 89.75 | 88.81  |
| WLK[19]   | 86.15 | 86.38 | 87.25 | 87.53 |        |
| graph2vec [25] | 76.96 | 82.48 | 79.63 | 82.55 | 83.35  |
| sub2vec_0[5] | 68.31 | 69.65 | 68.98 | 72.20 | 74.50  |
| sub2vec_5[5] | 66.94 | 68.36 | 67.64 | 73.13 | 74.98  |

- • Looking at the performances of baselines, one could see all of them perform reasonably better in the batch learning setting than the online setting. This is owing to their inability to handle vocabulary expansion which renders their models obsolete over time. Besides, none of them posses multi-view and semi-supervised learning potentials which could explain their overall substandard results.
- • Due to poor space complexity, GE-FSG [45] is unable to handle the large graphs used in this experiment and went OOM during the FSG extraction process. Hence, its results are not reported in the table.

5.1.2 Graph clustering.

Dataset & experiments. We now evaluate apk2vec on two different graph clustering tasks. Firstly, in the malware familial clustering task, 5,560 apps from Drebin [27] collection are used. These apps belong to 179 malware families. Malware belonging to the same family are semantically similar as they perform similar attacks. Hence, we obtain the profiles of these apps and cluster them into 179 clusters using k-means algorithm. Profiles of samples belonging to same family are expected to end up in the same cluster.

The next task is clone detection which uses 280 apps from Chen et al.'s [29] work. The apps in this dataset belong to 100 clone groups, where each group contains at least two apps that are semantic clones of each other with slight modifications/enhancements. Hence, in this task, we obtain the app profiles and cluster them into 100 clusters using k-means algorithm with the expectation that cloned apps end up in the same cluster.

Adjusted Rand Index (ARI) is used as a metric to determine the clustering accuracy in both these tasks.

Results & discussions. The clustering results are presented in Table 3. The following inferences are drawn from the table.

- At the outset, it is clear that apk2vec outperforms all the baselines on both these tasks. For familial clustering and clone detection, the improvements over the best performing baselines are 0.07 and 0.01 ARI, respectively.
- Interestingly, unlike malware detection not all the baselines offer agreeable performances in these two tasks. For instance, the ARIs of sub2vec and GE-FSG are too low to be considered as practically viable solutions. Given this context, apk2vec’s performances show that its embeddings generalize well and are task-agnostic.

5.1.3 Link prediction.

Dataset & experiments. For this task, we constructed an app recommendation dataset consisting of 2,318 apps downloaded from Google Play. We build a recommendation graph \( R \), with these apps as nodes. An edge is placed between a pair of apps in \( R \), if Google Play recommends one of them while viewing the other. With this graph, we follow the procedure mentioned in [8] to cast app
Table 3: Malware familial clustering and clone detection (graph clustering) results

| Technique  | Familiar clustering (ARI) | Clone detection (ARI) |
|------------|---------------------------|-----------------------|
| apk2vec    | 0.5124                    | 0.8360                |
| WLK[19]    | 0.3279                    | 0.7766                |
| graph2vec[25] | 0.4441                | 0.8272                |
| sub2vec[25] | 0.0374                    | 0.0180                |
| sub2vec_s[9] | 0.0945                | 0.0454                |
| GE-FSG [45] | OOM                      | 0.0171                |

Table 4: App recommendation (link prediction) results

| Technique  | AUC (P = 10%) | AUX (P = 20%) | AUX (P = 30%) |
|------------|---------------|---------------|---------------|
| apk2vec    | 0.7187        | 0.7347        | 0.7236        |
| WLK[19]    | 0.6643        | 0.6865        | 0.6805        |
| graph2vec[25] | 0.6803        | 0.7043        | 0.6767        |
| sub2vec[25] | 0.5446        | 0.5808        | 0.5603        |
| sub2vec_s[9] | 0.5206        | 0.5632        | 0.5631        |

Table 5: Clone detection results: single- vs. multi-view apk profiles

| Technique  | APIs(ARI) | Perm.(ARI) | Sink-sink(ARI) | concat.(ARI) | multi-view(ARI) |
|------------|-----------|------------|----------------|--------------|-----------------|
| apk2vec    | 0.8808    | 0.7762     | 0.7479         | 0.7766       | 0.8360          |
| WLK[19]    | 0.8678    | 0.7862     | 0.7479         | 0.7766       | -               |

Table 6: Impact of semi-supervised embedding on malware detection efficacy

| Labels($) | P($) | F($) | R($) | F($) |
|-----------|------|------|------|------|
| 0         | 94.71 | 96.99 | 97.11 | 96.27 |
| 10        | 95.44 | 97.11 | 96.27 | -     |
| 20        | 95.91 | 97.11 | 96.27 | -     |
| 30        | 96.59 | 97.11 | 96.27 | -     |

recommendation as a link prediction problem. That is, P, a subset of edges (chosen at random) are removed from R, while ensuring that this residual graph R’ remains connected. Now, given a pair of nodes in R’, we predict whether or not an edge exists between them. Here, endpoints of edges in P are considered as positive samples and pairs of nodes with no edge between them in R are considered as negative samples. We perform the experiment for P = {10%, 20%, 30%} of total number of edges in R.

Area under the ROC curve (AUC) is used as a metric to quantify the efficacy of link prediction.

**Results & discussions.** The results of the app recommendation task are presented in Table 4 from which the following inferences are drawn:

- For all values of P, apk2vec consistently outperforms all the baselines. Also, apk2vec’s margin of improvement over baselines is consistent and much higher in this task than graph classification and clustering tasks. For instance, it improves best baseline performances by 3 to 4% across all P values.

- It is noted that link prediction task does not involve any semi-supervision and hence all this improvement could be attributed to apk2vec’s multi-view and data-driven embedding capabilities. In sum, apk2vec consistently offers the best results across all the five tasks reported above. This illustrates that apk2vec’s embeddings are truly task-agnostic and capture the app semantics well.

5.2 Single- vs. multi-view profiles

In this experiment, we intend to evaluate the following: (i) significance of three individual views used in apk2vec, (ii) significance of concatenating app profiles from individual views (i.e., linear combination), and (iii) whether non-linear combination of multiple views is better than (i) and (ii).

**Dataset & experiments.** To this end, we use the clone detection experiment reported in §5.1.2. First, we build the app profiles (i.e., 64-dimensional embedding) with individual views (i.e., only one output layer is used in skipgram). Clone detection is then performed with each view’s profile. Also, we concatenate the profiles from three views to obtain a 192-dimensional embedding and perform clone detection with the same. Finally, the regular 64-dimensional multi-view embedding from apk2vec is also used for clone detection. Due to space constraints, from this experiment onwards, only WLK is considered for comparative evaluation, as it offers the most consistent performance among the baselines considered.

**Results & discussions.** The results of this experiment are reported in Table 5. The following inferences are drawn from the table:

- At the outset, it is evident that individual views are capable of providing reasonable accuracies (i.e., 0.70+ ARI). This reveals that individual views possess capabilities to retain different, yet useful program semantics.

- Out of the individual views, as expected, API view yields the best accuracy. This could be attributed to fact that this view extracts much larger number of high-quality features compared to the other two views. Owing to this well-known inference, many works in the past (e.g., [23, 27, 32, 36, 37]) have used them for a variety of tasks (incl. malware and clone detection). Also, source-sink view extract too few features to perform useful learning. In other words, it ends up underfitting the task. These observations are inline with the existing work on multi-view learning such as [24].

- In the case of WLK, API profiles gets a very high accuracy and when they are concatenated with other views, the accuracy is reduced. We believe this is due to the inherent linearity in this mode of combination i.e., views do not complement each other.

- Interestingly, in the case of apk2vec, concatenating profiles from individual views yields higher accuracy than using just one view. This reveals that using multiple views is indeed offering richer semantics and helps to improve accuracy. However, concatenation could only facilitate a linear combination of views and hence is yielding slightly lesser accuracy than apk2vec’s multi-view profiles. This illustrates the need for performing a non-linear combination of the semantic views.

5.3 Semi-supervised vs. unsupervised profiling

In this experiment, we intend to study the impact of using the (available) class labels of apps during profiling.

**Dataset & experiments.** Here, we use the same dataset which was used for online malware detection reported in §5.1.1. However, in order to study the impact of varying levels of supervision, we use...
labels for the following percentages of samples: 10%, 20%, and 30%. Profiles for apps are built with aforementioned levels of supervision and for each setting an SVM classifier is trained and evaluated for malware detection (other settings such as train/test split are similar to §5.1.1).

Results & discussions. The results of this experiment are reported in Table 6, from which the following inferences are made:

- One could observe that leveraging semi-supervision during apk2vec’s embedding is indeed helpful in improving the accuracy of the downstream task. For instance, using labels for merely 10% of samples help to improve the accuracy for malware detection by more than 2%.
- Clearly, using 30% labels yields better results than using just 10% and 20% labels. This illustrates the fact that the more the supervision is, the better the accuracy would be.
- In the case of WLK which uses handcrafted features, one could not use labels or other form of supervision to obtain graph embeddings. Hence, without any supervision, it performs reasonably well to obtain an f-measure of more than 93%. However, apk2vec with even just 10% supervision is able to outperform WLK significantly i.e., by nearly 3% f-measure.

5.4 Parameter Sensitivity

The apk2vec framework involves a number of hyperparameters such as embedding dimensions (δ), number of hash buckets (B) and number of hash functions (k). In this subsection, we examine how the different choices of δ affects apk2vec’s accuracy and efficiency, as it is the most influential hyperparameter. For the sensitivity analysis with respect to B and k, we refer the reader to the online appendix at [22].

Dataset & experiments. Here, the clone detection experiment reported in §5.1.2 is reused. The sensitivity results are fairly consistent on the remaining tasks reported in §5.1. Except for the parameter being tested, all other parameters assume default values. Embeddings’ accuracy and efficiency are determined by ARI and pretraining durations (averaged over all epochs), respectively.

Results & discussions. These results are reported in Figure 3 from which the following inference are drawn.

- Unsurprisingly, the ARI values increase with δ. This is understandable as larger embedding sizes offer better room for learning more features. However, the performance tends to saturate once the δ is around 500 or larger. This observation is consistent with other graph substructure embedding approaches [7, 8, 11].
- Also, the average pretraining time taken per epoch increases with δ. This is expected, since increasing δ would result in an exponential increase in skipgram computations. This is reflected in the exponential increase in pretraining time (especially, when δ > 500). This analysis helps in understanding the trade-off between apk2vec’s accuracy and efficiency for a given dataset and picking the optimal value for δ.

6 CONCLUSIONS

In this paper, we presented apk2vec, semi-supervised multimodal RL technique to automatically build data-driven behavior profiles of Android apps. Through our large-scale experiments with more than 42,000 apps, we demonstrate that profiles generated by apk2vec are task agnostic and outperform existing approaches on several tasks such as malware detection, familial clustering, clone detection and app recommendation. Our semi-supervised multimodal embeddings also prove to provide significant advantages over their unsupervised and unimodal counterparts. All the code and data used within this work is made available at [22].

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