Spin-one dark matter and gamma ray signals from the galactic center

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ABSTRACT: In this work we study the possibility that the gamma ray excess (GRE) at the Milky Way galactic center come from the annihilation of dark matter with a (1, 0) ⊕ (0, 1) space-time structure (spin-one dark matter, SODM). We calculate the production of prompt photons from initial state radiation, internal bremsstrahlung, final state radiation including the emission from the decay products of the μ, τ or hadronization of quarks. Next we study the delayed photon emission from the inverse Compton scattering (ICS) of electrons (produced directly or in the prompt decay of μ, τ leptons or in the hadronization of quarks produced in the annihilation of SODM) with the cosmic microwave background or starlight. All these mechanisms yield significant contributions only for Higgs resonant exchange, i.e. for $M \approx M_H/2$, and the results depend on the Higgs scalar coupling to SODM, $g_s$. The dominant mechanism at the GRE bump is the prompt photon production in the hadronization of $b$ quarks produced in $DD \rightarrow bb$, whereas the delayed photon emission from the ICS of electrons coming from the hadronization of $b$ quarks produced in the same reaction dominates at low energies ($\omega < 0.3 \text{ GeV}$) and prompt photons from $c$ and $\tau$, as well as from internal bremsstrahlung, yield competitive contributions at the end point of the spectrum ($\omega \geq 30 \text{ GeV}$).

Taking into account all these contributions, our results for photons produced in the annihilation of SODM are in good agreement with the GRE data for $g_s \in [0.98, 1.01] \times 10^{-3}$ and $M \in [62.470, 62.505] \text{ GeV}$. We study the consistency of the corresponding results for the dark matter relic density, the spin-independent dark matter-nucleon cross-section $\sigma_p$ and the cross section for the annihilation of dark matter into $bb$, $\tau^+\tau^-$, $\mu^+\mu^-$ and $\gamma\gamma$, taking into account the Higgs resonance effects, finding consistent results in all cases.

KEYWORDS: Cosmology of Theories beyond the SM, Effective Field Theories, Space-Time Symmetries

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1 Introduction

The understanding of the nature of dark matter is presently one of the major challenges in particle physics, astrophysics and cosmology. Dark matter amounts for 26% of the content of the universe and there is compelling evidence for its existence from the measurements of several independent observables, among which we have galaxy rotation curves, cosmic microwave background and dark matter relic density (for a recent review with a comprehensive list of references see [1]).

The measured dark matter relic density [2] can be obtained from its thermal decoupling from the primordial plasma. This requires \( \langle \sigma v \rangle \approx 10^{-9} \text{GeV}^{-2} \approx 10^{-26} \text{cm}^3/\text{seg} \), i.e. of the order of the weak scale cross sections, and a mass of the order of a hundred GeV for the so called weakly interactive massive particle (WIMP). This result can be understood in terms of the exchange of a massive particle between dark matter and standard model (SM) fields, with couplings of the order of the weak interactions, which points to the unification route, i.e. to identify dark matter with particles arising in formalisms unifying the three
interactions of the SM or including gravity with a wide variety of models yielding candidates with different space-time structures. Recently, a thorough study of the possibilities for scalar, fermionic and vector dark matter was done in [3], concluding that little room is left by available data for WIMPs with these space-time structures (see however [4]).

The SM uses only a very restricted set of the Homogeneous Lorentz Group (HLG) irreducible representations (irreps). Indeed, from the isomorphism of the HLG with SU(2) SU(2), the irreps of the HLG can be labelled by two SU(2) quantum numbers \((a,b)\). The SM uses only the scalar irrep, \((0,0)\), for the Higgs, the spin 1/2 chiral representations \((\frac{1}{2},0)\) and \((0,\frac{1}{2})\), for quarks and leptons and the vector irrep, \((\frac{1}{2},\frac{1}{2})\), for the gauge fields. Quantum field theory proposals for physics beyond the SM in general use these very same representations for their field content, except for supergravity which includes the gravitino transforming in the \((1,\frac{1}{2})\) representation and the graviton transforming in the \((1,1)\) representation.

In ref. [5] we proposed an alternative \((1,0)\oplus(0,1)\) space-time structure for dark matter, in a formalism that generalizes the structure of spin 1/2 Dirac theory to spin-one matter particles. The corresponding quantum field theory was developed in [6] and it is based in the parity-based construction of a covariant basis for \((j,0)\oplus(0,j)\) fields done in [7]. Spin-one matter fields are described by a six-component spinor and can be endowed with a vector gauge structure (the kinetic term is not chiral thus chiral gauge interactions are not permitted). The interaction of spin-one dark matter (SODM) with SM fields is constructed under the effective field theory philosophy and a basic principle: SM fields are singlets of the dark gauge group and vice versa. Considering for simplicity the dark gauge group as \(U(1)_D\), the leading interacting terms in the effective field theory are [5]

\[
\mathcal{L}_{\text{int}} = \bar{\psi}(g_s \mathbf{1} + ig_p \chi)\psi \phi + g_t \bar{\psi} M_{\mu\nu} \psi B^{\mu\nu} + \mathcal{L}_{\text{self int}},
\]

where \(g_s\), \(g_p\) and \(g_t\) are low energy constants. The self-interaction terms \(\mathcal{L}_{\text{self int}}\) are given in [6] and are not relevant for the purposes of this work. After spontaneous symmetry breaking, this Lagrangian yields

\[
\mathcal{L}_{\text{int}} = \frac{1}{2} \bar{\psi}(g_s \mathbf{1} + ig_p \chi)\psi (H + v)^2 + g_t C_W \bar{\psi} M_{\mu\nu} \psi F^{\mu\nu} - g_t S_W \bar{\psi} M_{\mu\nu} \psi Z^{\mu\nu},
\]

where \(C_W\), \(S_W\), \(H\), \(v\), \(F^{\mu\nu}\), \(Z^{\mu\nu}\) are the cosine and sine of the Weinberg angle, the Higgs field, the Higgs vacuum expectation value and the electromagnetic and \(Z^0\) strength tensors, respectively. The interacting terms include a spin portal (photon and \(Z^0\) coupling to higher multipoles of dark matter), a Higgs portal with a scalar and a parity-violating pseudo-scalar interaction, and a dark matter - anti-dark matter to two Higgs interaction.

Light dark matter \((M < M_Z/2)\) turns out to be inconsistent with the measured relic density and the generated invisible widths of the \(Z^0\) and Higgs boson. The upper bounds for the thermal average \(\langle \sigma v \rangle\) for \(DD \rightarrow bb, \tau^+\tau^-\) extracted by the FermiLAT-DES collaboration in the analysis of photon signals coming from Milky Way dwarf spheroidal satellite galaxies [8, 9] are well satisfied. On the direct detection side, the appropriate description of XENON1T measurement of \(\sigma_p\) [10] requires spin portal coupling \(g_t \leq 10^{-5}\) for \(M \approx 100\ GeV\) to \(g_t \leq 10^{-3}\) for \(M \approx 1\ TeV\). Less stringent upper bounds are obtained for the Higgs portal coupling \(g_s \leq 10^{-2}\) and no significant constraint is obtained for \(g_p\) [5].
In this formalism, the annihilation of spin-one dark matter into final states containing photons occurs at tree level which can be relevant for the search of gamma rays coming from the annihilation of dark matter. Gamma ray searches started a new era with the launch of PAMELA [11], AMS-02 [12], and the Large Area Telescope of the Fermi experiment (FermiLAT) [13]. Presently, strong upper limits have been obtained by these collaborations for the annihilation of dark matter into SM particles, which are complementary to searches at higher energies in experiments like HESS [14].

In the present work we study photon signals from the annihilation of SODM and the possible contributions of the corresponding mechanism to the gamma ray excess (GRE) from the galactic center claimed by several collaborations. The next section is devoted to the definition of the observables and conventions in this work and to the key observation that SODM yield annihilation cross sections of the order of the expected by recent fit to the GRE only at the Higgs resonance. In section 3 we study the mechanisms for the production of prompt photons in the annihilation of SODM. In section 4 we work out the production of gamma rays from inverse Compton scattering of electrons produced directly or indirectly in the annihilation of SODM. In section 5 we give our final results for this study. The consistency of our results with existing constraints on several observables is analyzed in section 6. Finally, our conclusions are given in section 7.

2 Gamma ray excess from the galactic center

2.1 GRE, prompt photons and muon inverse Compton scattering

During the past few years, it has been claimed by several groups that an excess over the expected gamma ray flux from known sources in the Milky Way galactic center exists in the FermiLAT data around 3 GeV [15–25]. The large uncertainties involved in the interpretation of FermiLAT data have been recently analyzed by the FermiLAT collaboration [26] concluding that a GRE excess in a region around 3 GeV indeed exists, but a broad band of possible values for the corresponding differential flux as a function of the photon energy is permitted by these uncertainties. Although the GRE can be explained by little known astrophysical sources [15, 27–31], the annihilation of dark matter into final states containing photons remains as an attractive possibility [4, 21, 32–40] and we work out here the results for dark matter with a $(1, 0) \oplus (0, 1)$ space-time structure.

The gamma ray differential flux from the annihilation of (non-self-conjugated) dark matter is

$$\frac{d\Phi}{d\omega} = \left( \sum_i \frac{B_i}{16\pi M^2} \frac{d\langle \sigma v \rangle^i_\gamma}{d\omega} \right) \int_{\Delta\Omega} \int_{\Delta s} \rho^2(r(s, \theta)) ds d\Omega. \quad (2.1)$$

The sum runs over all annihilation channels containing at least one photon in the final state; $\frac{d\langle \sigma v \rangle^i_\gamma}{d\omega}$ is the velocity averaged differential cross section for the $i$-channel and $B_i$ is the number of photons produced in this process. In the literature, the differential photon flux in eq. (2.1) is sometimes written in terms of the spectrum for each channel

$$\frac{dN^i_\gamma}{d\omega} = \frac{1}{\langle \sigma v \rangle_i} \frac{d\langle \sigma v \rangle^i_\gamma}{d\omega}, \quad (2.2)$$
where \(\langle \sigma v_r \rangle_i\) stands for the non-radiative cross section for the \(i\)-channel. It is conventionally assumed that this non-radiative cross section contains all the information on the annihilation of dark matter entering the radiative process, in such a way that the spectrum has the information of the photon production from standard model \(i\)-states which can be calculated and, beyond technical details, it is well known. In this construction, model independent fits to data can be done with \(\langle \sigma v_r \rangle_i\) and \(M\) as free parameters.

The term in the parentheses in eq. (2.1) contains all the information from the dark matter interactions and the integral contains the so called \(J\)-factor for the observation window defined by the solid angle

\[
J(\Delta \Omega) = \int_{\Delta \Omega} \int_{\Omega_{\text{obs}}} \rho^2(r(s, \theta)) dsd\Omega.
\]

(2.3)

In the computations in this work, unless otherwise explicitly stated, we will use the generalized Navarro-Frenk-White (gNFW) dark matter profile

\[
\rho(r) = \rho_s \frac{r_s^3}{r^{\gamma}(r + r_s)^{3-\gamma}}
\]

(2.4)

with the values \(r_s = 20\) kpc for the scale radius, \(\gamma = 1.25\) for the slope of the inner part of the profile. The scale density \(\rho_s = 0.225\) GeV/cm\(^3\) is fixed by requiring the local dark matter density at \(r_\odot = 8.5\) kpc to be \(\rho_\odot = 0.4\) GeV/cm\(^3\).

The production of prompt gamma rays in the annihilation of dark matter into \(\bar{q}q, \bar{c}c, \bar{b}b, e^+e^-, \mu^+\mu^-, \tau^+\tau^-, W^+W^-, ZZ, hh, gg\) was fitted to the FermiLAT data for the GRE in [37], finding in general that the GRE can be explained if dark matter annihilates into any of these pairs of particles except for the \(e^+e^-\) channel, whenever the dark matter mass is in the range 5 – 174 GeV depending on the specific channel, and the corresponding cross section is of the order of the thermal one, \(\langle \sigma v_r \rangle \approx 10^{-26} \text{cm}^3/\text{seg}\). In particular, the annihilation into fermionic states, \(\bar{D}D \to \bar{f}f\) with \(f = \mu, \tau, q, c, b\) yields good fits to the GRE data for dark matter mass in the 9 – 61 GeV range.

Another possible mechanism to explain the GRE is the production of gamma rays in the Inverse Compton Scattering (ICS) of electrons and muons produced in dark matter annihilation into \(e^+e^-\) and \(\mu^+\mu^-\), which propagates over the galactic center and scatter photons from the Cosmic Microwave Background (CMB) or starlight [36]. The electronic channel for electrons produced directly in the annihilation of dark matter into \(e^+e^-\) requires a large annihilation cross section \(\langle \sigma v_r \rangle_e\) which is severely constrained by the positron fraction data from the AMS Collaboration [41, 42]. In [37], it was shown that the muon channel yield sizable contributions to the GRE and when added to the prompt photon production in this channel allows for higher values of the dark matter mass \((M \approx 61\text{ GeV})\), with the required cross section still being of the order of the thermal cross section.

### 2.2 Spin-one dark matter annihilation into fermions and the GRE

The interactions of SODM with SM fields in eq. (1.2) allow for the annihilation of dark matter into all the channels mentioned above except for the \(gg\) channel. The cross-section
for the annihilation of SODM into a fermion pair, worked out in [5], is

\[
\langle \sigma v_r \rangle_f (s) = \frac{1}{144\pi M^4 \sqrt{s}} \left[ m_f^2 \left( s - 4m_f^2 \right) \left( g_h^2 s (s - 4M^2) + g_w^2 (6M^4 - 4M^2 s + s^2) \right) \left( (s - M_H^2)^2 + \Gamma_H^2 M_H^2 \right) \right]
\]

\[
+ \frac{2g_h^2 m_Z^2 s (s - 4M^2) (2M^2 + s) \left( 2 \left( A_f^2 - 2B_f^2 \right) m_f^2 + s \left( A_f^2 + B_f^2 \right) \right)}{3v^2 \left( (s - M_Z^2)^2 + \Gamma_Z^2 M_Z^2 \right)^2}
\]

\[
+ \frac{32C_W^2 Q_f^2 g_W^2 M_W^2 \left( s - 4M^2 \right) (2M^2 + s) \left( 2m_f^2 + s \right)}{3v^2 s}
\]

\[
- \frac{16A_f C_W Q_f g_W^2 M_W^2 M_Z^2 s (s - 4M^2) (2M^2 + s) \left( 2m_f^2 + s \right)}{3v^2 \left( (s - M_Z^2)^2 + \Gamma_Z^2 M_Z^2 \right)} \right].
\]

(2.5)

where \( m_f, Q_f \) correspond to the mass of the fermion and its charge in units of \( e > 0 \), respectively, and

\[
A_f = 2T_f^{(3)} - 4Q_f \sin^2 \theta_W, \quad B_f = -2T_f^{(3)}.
\]

The non-relativistic expansion of the cross section, averaged in the velocity yields

\[
\langle \sigma v_r \rangle_f = \frac{N_c g^2 m_f^2 (M^2 - m_f^2) s}{12\pi M^3 (4M^2 - M_H^2)^2 + M_H^2 \Gamma_H^2}.
\]

(2.7)

where \( N_c = 3 \) for quarks and \( N_c = 1 \) for leptons. In figure 1 we give the detail of the velocity averaged cross sections for \( f = \mu, \tau, c, b \), as well as the thermal cross section close to the resonance region, outside of which it takes negligible values. It is clear from this plot that only for SODM mass in the Higgs resonance region, \( M \approx M_H/2 \), we get values of the order of the thermal cross section. In the case \( f = \mu, \) even at the peak of the resonance we get very small values \( \langle \sigma v_r \rangle_e = 1.3 \times 10^{-30} \text{cm}^3/\text{s} \).

The sharp prediction \( M \approx M_H/2 \) for the dark matter mass suggested by the comparison of the annihilation of SODM into fermions with the required cross sections in the fit to the GRE data done in [37] is interesting and deserves a complete analysis of the photon signals produced in the annihilation of SODM into SM particles. The contributions of a Higgs portal to the GRE have been studied previously in the literature for dark matter with a scalar (0, 0), four-vector (1/2, 1/2), or spinor (1/2, 0) \( \oplus (0, 1/2) \), space-time structures [21, 32–35, 38–40], mainly in the context of models of minimal scalar dark matter to which fermions or vectors are sometimes added in several set ups to comply with available data on dark matter. The possibility that a dark matter with a mass around half the Higgs mass could explain the GRE for singlet scalar dark matter has also been pointed out in [4, 38–40].

In the next sections we analyze the prompt photon production from the annihilation of SODM into fermions, and the delayed photon emission from electrons and muons produced in the decay of \( q, \tau, c \) and \( b \), which propagates in the galactic center interacting with the cosmic microwave background and starlight. We take into account all these contributions to find the window for the SODM mass and couplings consistent with the GRE and uncertainties presented in [26]. Finally we analyze the consistency of the so obtained results with the constraints from direct and indirect detection for SODM in the Higgs resonance region.
Figure 1. Detail of $\langle \sigma v_r \rangle_f$ for the annihilation of SODM into fermions close to the Higgs resonance for $g_s = 2 \times 10^{-3}$ as a function of the SODM mass. The orange line corresponds to the thermal cross section [43].

3 Prompt photons from the annihilation of SODM into fermions

The couplings $g_s, g_p, g_t$ in eq. (1.2) induce the annihilation of SODM into final states containing photons which we classify as initial state radiation, internal Bremsstrahlung (or internal radiation) and final state radiation. The simplest transitions are the two-body processes $\bar{D}D \rightarrow \gamma R$ with $R = \gamma, Z^0$ whose amplitudes are $\mathcal{O}(g^2_t)$ or $R = H$ which is $\mathcal{O}(g_t g_s g_p)$. Considering non-perturbative QCD corrections in general $R$ in these processes can convert to quarkonium state resonances $\bar{Q}Q^{[2S+1LJ]}$ producing also $\gamma$-quarkonium final two body states. These two body processes yield photons with energies in a narrow energy window related to the width of the resonance $R$ and centered at $\omega = M(1 - \frac{M_R^2}{4M_T^2})$. These contributions dominate the related three-body final state processes obtained considering the decay of $R$ into two particles, which have a continuous photon spectrum produced when $R$ is off-shell. This is the so-called initial state radiation. Since the three-body process in general includes the two body transitions as resonant processes we consider here the general case of three body transitions containing a photon in the final state. For three body transitions it is also possible that the SODM annihilates into a pair of particle-antiparticle with the subsequent emission of a photon, this is final state radiation. It is also well possible that the exchanged particle $R$ decay into another particle $R'$ emitting a photon with the subsequent decay of $R'$ into two final particles in the so called internal radiation or internal bremsstrahlung. The corresponding diagrams for SODM transitions $\bar{D}D \rightarrow \bar{f}f\gamma$, where $f$ stands for a fermion, are depicted in figure 2.
3.1 Initial state radiation

Initial state radiation is induced at tree level by the first two diagrams in figure 2. It is well known that initial state radiation yields spectrums with shape similar to the GRE when there are resonant effects involved in the process. In this case the resonant effects translate into wider peaks in the photon spectrum (see e.g. [44] for these effects in colliders at low energies). The first diagram in figure 2 (γ and Z exchange) yield contributions of order $O(v^2)$ and initial state radiation is dominated by the Higgs exchange in the second diagram. We obtain

$$\frac{d\langle v_r\rangle_{isr}}{d\omega} = \sum_f \frac{N_c \cos^2 \theta_W g_f^2 m_f^2 \omega (M - \omega) \left(1 - \frac{m_f^2}{M(M-M)}\right)^{3/2}}{72\pi^3 M^5} \times \frac{9g_\gamma^2 \omega^2 + g_Z^2 (2M + \omega)^2}{(4M(M - \omega) - M_{H_2}^2)^2 + \Gamma_{H_2}^2 M_{H_2}^2},$$

where the sum runs over all kinematically allowed SM fermions. As expected, for $M > M_{1/2}$ the photon spectrum has a bump at energies corresponding to di-fermion invariant mass close to the Higgs resonance. The location of this bump depends on the dark matter mass and for $M = 64 GeV$ it coincides with the GRE bump at $3 GeV$. However, this is an $O(g_t g_s^2)$ contribution to the cross-section. The coupling $g_t$ is severely constrained to

Figure 2. Anihilation of SODM into three body final states containing a photon. There is an additional diagram for each one shown here.
Figure 3. Differential photon flux for final state radiation as a function of $\omega, M$ for $g_s = 5 \times 10^{-3}$.

$g_t \leq 2 \times 10^{-4}$ by the XENON1T results on direct detection for SODM mass of the order of 100 GeV [5], which makes the initial state radiation very small compared with the GRE data.

3.2 Final state radiation

Prompt photons can be also emitted by the final fermions in the reaction $\bar{D}D \rightarrow f\bar{f}\gamma$. These contributions are given by the next two diagrams in figure 2. The $\gamma$ and $Z$ exchange and the Higgs exchange with pseudoscalar coupling $g_p$ are $O(v^2_r)$. The leading contributions are given by the diagrams with the Higgs exchange and scalar coupling. The differential averaged cross section is

$$
\frac{d(\sigma v_r)_{fsr}}{d\omega} = \sum_f \frac{N_c \alpha Q_f^2 g_s^2 m_f^2}{6\pi^2 M^4 \omega \left( (4M^2 - M_H^2)^2 + \Gamma_H^2 M_H^2 \right)} \\
\times \left[ 2M^3 (M - \omega) + M^2 (\omega^2 - 3m_f^2) + 2Mm_f^2 \omega + m_f^2 \right] \text{Arctanh} \sqrt{1 - \frac{m_f^2}{M(M - \omega)}} \\
\times \left[ -M(M^2 - m_f^2)(M - \omega) \sqrt{1 - \frac{m_f^2}{M(M - \omega)}} \right].
$$

(3.2)

The corresponding differential photon flux as a function of the dark matter mass is shown in figure 3. These contributions are also resonant but in this case the resonant effects occur exactly at

$$
s = (p_1 + p_2)^2 = 4M^2 \left( 1 + \frac{v_r^2}{4} + O(v_r^4) \right)^2 = M_H^2.
$$

(3.3)

From this plot it is clear that results for $\omega^2 d\Phi/d\omega$ of the order of the GRE are obtained only for Higgs exchange in the resonance region. Since dark matter is non-relativistic, this requires $M \approx M_H/2$. 

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The direct emission of a photon by the fermion produced in SODM annihilation is only one of the many processes yielding prompt photons. For \( f = \mu, \tau, q, c, b \) additional prompt photons can be produced by the decay products in the case of leptons or by the jet of particles produced in the hadronization of quarks. We expect these effects to modify substantially our results in eq. (3.2) for all fermions except for \( f = e, \mu \) which do not have hadronic decays and receive only modifications from suppressed higher order electroweak radiative corrections.

We calculate the complete prompt photon flux for \( f = e, \mu, \tau, q, c, b \) using the tabulated spectrum defined as provided by DARKSUSY [45] and PPC4DMID [46], including radiative corrections [47]. We check the consistency of results using both packages and use the spectrum given by the direct photon emission by electrons and muons in eq. (3.2) to cross-check results. The comparison of the direct photon emission in eq. (3.2) versus the tabulated spectrum from PPC4DMID are shown in figure 4, which confirms our expectations.

The prompt photon flux is calculated using the tabulated spectrum in PPC4DMID (DARKSUSY yields similar results) and the SODM result for \( \langle \sigma v_r \rangle_{ff} \) in eq. (2.7) for each fermion. Our results for \( g_s = 10^{-3} \) and \( M = 62.49 \text{GeV} \) are shown in figure 5. In the computation of the flux we use the gNFW profile [48, 49] with \( \gamma = 1.25 \) which for the region of interest \( |l| < 10^9 \) and \( 2^0 \leq |b| < 10^6 \) yields \( J_0 = 7.12 \times 10^5 \text{GeV}^4/\text{cm}^2 \text{ seg} \).

The most important contributions comes from the \( b \) channel followed by the \( c \) and \( \tau \) which become competitive at high photon energies. Prompt photon flux from electrons muons and light quarks turn out to be negligible.

Figure 4. Comparison of the tree level result in eq. (3.2) for \( \frac{dN_f}{d \omega} (\text{GeV}^{-1}) \) versus the results using PPC4DMID tabulated spectrum, for leptons and quarks, as a function of \( \omega \) for \( M = 62.5 \text{GeV} \).
Figure 5. Differential flux for prompt photons from the annihilation of SODM into fermions for $M = 62.49 \text{GeV}$ and $g_s = 10^{-3}$. We use $M_H = 125.09 (\text{GeV})$ in the computation of these contributions.

3.3 Internal Bremsstrahlung

The internal state radiation is given by the last two diagrams of figure 2. The first of these diagrams involve the $H \rightarrow \gamma\gamma$ and $H \rightarrow Z\gamma$ transitions which takes place at one-loop level in the standard model. The $H\gamma\gamma$ and $H\gamma Z$ three-point functions have been calculated in the literature [50–52]. Considering only the parts contributing to our processes, the SM yields the following effective interactions

$$\mathcal{L}_{\text{eff}} = H[G_{\gamma\gamma} F_{\mu\nu} F_{\mu\nu} + G_{Z\gamma} F^{\mu\nu} Z_{\mu\nu}], \quad (3.4)$$

where $G_{\gamma\gamma}, G_{Z\gamma}$ are the corresponding form factors. We will follow a phenomenological approach here, and normalizing the form factors as $G_{\gamma\gamma} = \frac{g_{\gamma\gamma}}{M_H}$, $G_{Z\gamma} = \frac{g_{Z\gamma}}{M_H}$, will extract the couplings from the measured branching ratios $BR[H \rightarrow \gamma\gamma] = 2.27 \times 10^{-3}$, $BR[H \rightarrow Z\gamma] = 1.53 \times 10^{-3}$ [2] to obtain $g_{\gamma\gamma} = 1.91 \times 10^{-3}$, $g_{Z\gamma} = 3.30 \times 10^{-3}$. These couplings correspond to the form factors for on-shell momentum. As it will be shown below, only the resonant processes produce sizable contributions for most of the channels relevant in this work, hence this approximation is justified for our purposes.
For the sequential decay with $\gamma$ and $Z^0$ intermediate states we obtain

$$\langle d\sigma_{\gamma^*} \rangle_{Z^0} = \sum_f \frac{N_c g_Z^2 g^2 \omega^3 M_Z^2 \sqrt{1 - \frac{m_f^2}{M(M - \omega)}}}{36 \pi^2 M_H^2 \left[ (4M^2 - M_Z^2)^2 + \Gamma_H^2 M_H^2 \right]} \times 2(A_f^2 + B_f^2) M(M - \omega) + (A_f^2 - 2B_f^2) m_f^2 \left[ (4M - \omega) - M_Z^2 \right]^2 + M_Z^2 \Gamma_H^2 \right), \quad (3.5)$$

$$\langle d\sigma_{\gamma^*} \rangle_{\gamma^*} = \sum_f \frac{N_c g_W^2 g^2 \omega^3 M_W^2 \sqrt{1 - \frac{m_f^2}{M(M - \omega)}}}{36 \pi^2 M_H^2 \left[ (4M^2 - M_W^2)^2 + \Gamma_H^2 M_H^2 \right]} \times \omega^3 \left[ 2M(M - \omega) + m_f^2 \right] \sqrt{1 - \frac{m_f^2}{M(M - \omega)}} \right). \quad (3.6)$$

There is also an enhancement at the Higgs resonance in these processes and a double-resonant effect in the case of the $Z^0$ intermediate state. The last diagram in figure 2 involves non-perturbative QCD effects. We calculated these contributions using the Non-Relativistic QCD effective field theory finding them negligible even at the Higgs resonance.

There are also contributions with the sequential decays $\bar{D}D \rightarrow \gamma^* Z^0 \rightarrow H \gamma^* f f$ not shown in figure 2 which are not resonant and are also very small.

Our results for the internal radiation are shown in figure 5. Sizable contributions to the differential photon flux from $H \rightarrow \gamma Z^*$ transition are produced mainly at the $Z^0$ resonance i.e. for photon energies around $\omega = \frac{M_H}{2} \left[ 1 - \frac{M_Z^2}{M_H^2} \right] \approx 30 \text{ GeV}$. The $H \rightarrow \gamma \gamma^*$ intermediate state contributes only at the upper end of the spectrum.

4 Delayed emission: inverse Compton scattering contributions

There are at least three different contributions from the delayed photon emission by ICS of propagating fermions produced in the annihilation of SODM: i) The propagation of electrons produced in $\bar{D}D \rightarrow e^+ e^-$, which is negligible due to the small coupling with the exchanged Higgs, $g_{Hee} = m_e/v$, or the small coupling of $\gamma$ and $Z$ to SODM (proportional to $g_t$) if we consider the spin portal; ii) The propagation of muons produced in $\bar{D}D \rightarrow \mu^+ \mu^-$ which was shown in [37] to yield sizable contributions; iii) The propagation of electrons coming from the decay of leptons or hadronization of quarks, produced in $\bar{D}D \rightarrow f f$ with $f = \mu, \tau, q, c, b$.

We compute the ICS of electrons by the cosmic microwave background or starlight for electrons produced in the decay of heavier leptons or in the hadronization of quarks using the tabulated electron spectrum and propagating models in PPC4DMID [46, 53]. Our results for the photon flux from the different fermions are given in figure 6. We warn that these contributions are calculated with the NFW [54] density profile since the PPC4DMID tabulated spectrum is designed only for specific profiles not including the gNFW. However, these contributions are not very sensitive to the density profile and results are quite similar using the Moore [55] or Einasto B [46, 56] profiles included in the PPC4DMID setup and are more alike to the gNFW used in the computation of prompt photons.
Figure 6. Differential flux of delayed photons produced in the ICS of electrons off CMB and starlight, for secondary electrons produced in the decay of heavier leptons or hadronization of quarks coming from the annihilation of SODM, for $M = 62.49\text{ GeV}$ and $g_s = 10^{-3}$. We use $M_H = 125.09\text{ (GeV)}$ in the computation of these contributions.

In this case also the $b$ channel is dominant, with subdominant contributions of the $c$ and $\tau$ channels, light quarks, with electrons and muons yielding negligible contributions. We remark that for both prompt and delayed photons, these contributions rise as we go deeper inside the resonance region, results being highly sensible to the specific value of the SODM mass.

There are also contributions to the delayed photon flux from the ICS of muons produced in $\bar{D}D \rightarrow \mu^+\mu^-$ calculated in [37]. However, for the SODM mass window required by the GRE data when we include all the contributions, the cross section $\langle \sigma v_r \rangle_\mu$ is about three orders of magnitude below the thermal cross section needed for this mechanism to yield a sizable contribution and the corresponding flux turns out to be very small.

5 Final results

Including all the contributions described in the previous section we obtain the results shown in figure 7. Although these results in principle depend on the SODM mass $M$ and on the couplings of the model $g_s, g_p, g_t$, the spin portal ($g_t$) and pseudoscalar ($g_p$) couplings yield negligible contributions to the photon flux which depends only on the parity-conserving Higgs-SODM interaction coupling $g_s$ and $M$.

As to the size of the individual contributions, we have a similar amount of prompt and delayed photons, but prompt photons are dominant for $\omega > 0.3\text{ GeV}$. In both cases, the
main contributions come from the $\bar{D}D \rightarrow \bar{b}b$ annihilation with small but sizable contributions from the $\tau^+\tau^-$ and $\bar{c}c$ channels. Among prompt photons most of the flux comes from final state radiation. Internal radiation yields competitive contributions only at the upper end of the spectrum.

In figure 7, we show also the shadowed band allowed by the uncertainties on the GRE data obtained in [26]. Considering these uncertainties we obtain the values $g_s \in [0.98, 1.01] \times 10^{-3}$ and $M \in [62.470, 62.505] \text{ GeV}$ consistent with the GRE data. These sharp set of values yield definite predictions for other observables of dark matter and we must ensure that existing constraints are satisfied. In the next section we work out the corresponding results for constraints from relic density, direct and indirect searches for dark matter.

6 Constraints from direct and indirect detection experiments at the Higgs resonance

A global analysis of the predictions of the formalism for results on the relic density, direct searches (XENON1T upper bound for the dark matter-proton cross section $\sigma_p$) and indirect searches (upper bounds on the annihilation of dark matter into $bb, \tau^+\tau^-, \mu^+\mu^-$) was performed in [5], finding consistency with available data. However, the sharp result on the SODM mass imposed by the GRE, requires a deeper analysis for a SODM mass at the Higgs resonance because, on the one hand, the non-relativistic approach used in the calculation of the dark matter relic density is well known to break down in the presence of
resonances, and on the other hand, the cross-sections for the annihilation of dark matter dramatically grow at the Higgs resonance and we must ensure that the annihilation cross section to fermions, specially to $\bar{b}b$, is consistent with present upper limits.

6.1 Direct detection

The XENON1T upper bound for $\sigma_p$ at $M = M_H/2$ is $\sigma_p \leq 9.86 \times 10^{-47} \text{cm}^2$. This upper bound requires $g_s \leq 5.12 \times 10^{-3}$ for the Higgs portal or $g_t \leq 1.7 \times 10^{-5}$ for the spin portal. The window $g_s \in [0.98, 1.01] \times 10^{-3}$ imposed by the GRE data is consistent with the upper bound on $g_s$ imposed by XENON1T.

6.2 Relic density

Our results for the dark matter relic density in [5] must be redefined if $M \approx M_H/2$, since we are at the Higgs resonance and it has been shown previously in a general analysis that the naive calculation of the dark matter relic density using the non-relativistic expansion can fail in the presence of resonances [57]. The scope of this failure depends on the specific values of the resonance mass and width, but it can be important well beyond the resonance region. Our model allows to test how important it can be for the Higgs resonance.

The calculation of the relic density requires to consider the full thermal average cross-section $\langle \sigma v_r \rangle(x)$ for the annihilation of dark matter into standard model states. For masses $M \approx M_H/2$, dark matter annihilates only into $ff$, $\gamma\gamma$ and $Z^0\gamma$. The cross section for the annihilation into light fermions is given in eq. (2.5).

The leading contributions for SODM annihilation into $\gamma\gamma$ and $Z^0\gamma$ via Higgs exchange are shown in figure 8 and involve next to leading order SM contributions inducing the $H \rightarrow \gamma\gamma$ and $H \rightarrow \gamma Z$ transitions. The spin portal contributions generated by the $g_t$ coupling turn out to be very small and the pseudoscalar Higgs portal induced by $g_p$ are $O(v_r^2)$, thus we keep only the scalar Higgs portal contributions given by $g_s$.

A straightforward calculation of $\bar{D}D \rightarrow \gamma\gamma$, $Z^0\gamma$ induced by Higgs exchange yields

$$\langle \sigma v_r \rangle_{\gamma\gamma} = \frac{g^2_{\gamma\gamma} g_s^2 v^2 s^2 (6M^4 - 4M^2 s + s^2)}{288\pi M^4 M^2 s^2 (s - 2M^2) |(s - M_H^2)^2 + M_H^4 |},$$ (6.1)

$$\langle \sigma v_r \rangle_{Z\gamma} = \frac{g^2_{Z\gamma} g_s^2 v^2 (s - M_Z^2)^2 (6M^4 - 4M^2 s + s^2)}{144\pi M^4 M^2 s (s - 2M^2) |(s - M_H^2)^2 + M_H^4 |}. \tag{6.2}$$

We use these results to calculate numerically the complete thermal average cross section. Our results compared with those obtained with the non-relativistic expansion are shown in figure 8.
in figure 9, where it can be seen that even for values of $M$ far from the resonance there are important differences and, at the resonance, these differences are dramatic and extend to the highly non relativistic regime. We use the complete function $h v r i(x)$ to solve the freezing condition and the Boltzmann equation for the relic density following the conventional procedure used in [5]. The freezing temperature is still around $x_f \approx 25$. The corresponding values of the coupling $g_s$ and the dark matter mass $M$ consistent with the measured relic density are shown in figure 10. Consistency with the XENON1T upper bounds on $\sigma_p$ holds only for a mass $M \in [60.05, 62.96]$ GeV and restricts the scalar coupling to values in the $g_s \in [0.95, 5.15] \times 10^{-3}$ window. These values are consistent with the GRE data which requires $g_s \in [0.98, 1.01] \times 10^{-3}$ and $M \in [62.47, 62.50]$ GeV, but the measured relic density correlates the values of these parameters to the solid curve in figure 10.

6.3 Annihilation into $\mu^+\mu^-$, $\tau^+\tau^-$ and $b\bar{b}$

Upper bounds for the $\mu$ channel were obtained in [41] as a function of the dark matter mass using the AMS02 data on the positron fraction in primary cosmic rays [42]. For $M = 62.5$ GeV the upper limit is $\langle \sigma v_r \rangle_\mu \leq 8.96 \times 10^{-26} cm^3/seg$ and this value is stable across the resonance region. For SODM the largest values of this cross section compatible with the GRE data is obtained for $M = 62.505$ GeV for which the measured relic density requires $g_s = 9.81 \times 10^{-4}$. A calculation of the SODM prediction with these values yields $\langle \sigma v_r \rangle_\mu \leq 8.30 \times 10^{-30} cm^3/seg$ well below the experimental upper bound.

As for the $\tau$ channel the upper limit obtained in [8] for $M = 62.5$ GeV is $\langle \sigma v_r \rangle_\tau \leq 1.2 \times 10^{-26} cm^3/seg$, while a calculation in our formalism of the largest value compatible with the GRE data yields $\langle \sigma v_r \rangle_\tau = 2.42 \times 10^{-27} cm^3/s$, consistent with the experimental upper bound.

The $b$ channel deserves a closer analysis since our results are near the upper bounds. In figure 11 we plot the median expected limit and the region for 95% containment obtained
Figure 10. Values of the coupling $g_s$ and SODM mass $M$ consistent with the measured relic density near the Higgs resonance obtained without the $v_r^2$ expansion (continuous line). The dashed line correspond to the conventional non-relativistic expansion. The short-dashed line is the upper bound on $g_s$ imposed by XENON1T results on $\sigma_p$ [5].

in [8] and our results for $\frac{1}{2}\langle\sigma v_r\rangle_\tau$ (the $\frac{1}{2}$ factor is required since the upper bounds are obtained for self-conjugated dark matter) . Although our results are consistent with the 95% containment band for the whole mass window compatible with the GRE, and below the median expected limit for a narrower mass window $M \in [62.470, 62.480]\, GeV$, it is important to analyze this compatibility in detail since, on the light of the results in the present work, this channel is a very promising place to look for signals of SODM. In this concern, it is important to remark that the Higgs is a very narrow resonance ($\Gamma_H/M_H = 3.2 \times 10^{-5}$), its energy resolution is not easy and even in collider experiments it is still a pending task.

The upper bounds as a function of the dark matter mass are obtained in [8, 9] from a combined analysis of the data on the energy flux from 45 dwarf spheroidal galaxies (dSph). Only 19 of these 45 targets have a $J$-factor derived from experimental data on stellar dynamics, a work done in [58], the fluxes for the remaining 26 targets are estimated from the empirical relation between the flux and the inverse square of the distance satisfied by the dSphs with flux derived from data on stellar dynamics.

For each target, the likelihood analysis performed for the photon energy flux consider 24 logarithmically spaced energy bins in the energy region from 500 $MeV$ to 500 $GeV$ using the likelihood function data provided in the supplementary material of [9]. Then the bin-by-bin upper bound for the photon flux excess at the 95% confidence level is calculated following the likelihood formalism described in [59]. These results are then used to estimate the upper bound on $\langle\sigma v_r\rangle_b$ for a given mass $M$ using the standard model results for the photon spectrum from $b$ quarks for each target and a combined likelihood analysis of these results yields the plot in figure 9 of [9].
In order to make a direct comparison of our results with experimental data, for each target, we reproduce the bin-by-bin upper bound for the photon flux excess at the 95% confidence level using the likelihood function data provided in the supplementary material of [9] and the likelihood formalism in [59]. Then we calculate the predictions of the formalism for the photon energy flux for each of the 19 targets. For given values of \( M \) and \( g_s \), we obtain the energy flux integrating the \( \bar{D}D \rightarrow \bar{b}b \) contribution to \( \omega \frac{d\Phi}{d\omega} \) bin-by-bin, where we use the J-factor of the considered target. We extrapolate these points to obtain the photon energy flux as a function of the photon energy. In figure 12 we show our results for the largest contribution obtained in our formalism consistent with the GRE data, corresponding to \( M = 62.505 \) (GeV) and \( g_s = 9.81 \times 10^{-4} \). We show also in figure 12 the band corresponding to the uncertainties in the measured J-factor of the target. In this plot we display only results for the 19 targets with J-factors derived from stelar dynamics data, but similar results are obtained for the rest of the targets. The photon energy flux from SODM annihilation into b-quark pairs, for each target, turns out to be smaller than the limits obtained using the bin-by-bin likelihood functions provided by FermiLAT-DES in the supplementary material of ref. [9].

6.4 Dark matter annihilation into two photons

There are stringent upper bounds on \( \langle \sigma v_r \rangle_{\gamma\gamma} \) by FermiLAT [60] and HESS [14] collaborations, which for \( M \approx M_H/2 \) are \( \langle \sigma v_r \rangle_{\gamma\gamma} \leq 6.75 \times 10^{-29} \text{cm}^3/\text{seg} \).
Figure 12. Energy flux (in units of $GeV \ cm^{-2} \ s^{-1}$) from each of the 19 targets whose J-factor was derived from stellar kinematics in [58] and were used in [9] to extract the upper bounds for the annihilation of dark matter into $b\bar{b}$. The colored dots represent the values of the likelihood function, where red is a higher value and blue is lower. The black solid line is the energy flux upper limit at 95% confidence level obtained from the bin-by-bin likelihood functions. The shaded white area represents the energy flux for SODM annihilating into b-quark pairs, using the measured J-factor and its uncertainty, for $M = 62.505 \ GeV$ and $g_s = 9.81 \times 10^{-4}$. The averaged cross section for the annihilation of SODM into two photons is given in eq. (6.1). A straightforward calculation to leading order in $v^2_r$ yields

$$
\langle\sigma v_r\rangle_{\gamma\gamma} = \frac{g_{\gamma\gamma}^2 g_s^2 M^2 v^2}{6\pi M_H^2 \left( (4M^2 - M_H^2)^2 + M_H^2 \Gamma_H^2 \right)}.
$$

In figure 13 we show the upper bounds obtained by FermiLAT [60] and our results for the window of SODM mass consistent with GRE data. In this case the predictions of our formalism are consistent with available data but also in this channel we are at edge of the allowed values for $\langle\sigma v_r\rangle_{\gamma\gamma}$ and lowering this upper bound could test the possibility that dark matter has a $(1, 0) \oplus (0, 1)$ space-time structure.
Figure 13. Annihilation cross section of SODM into two photons for $g_s = 9.81 \times 10^{-4}$ (solid line). The dashed line correspond to the upper limits and the shadow band to the 95% confidence level region obtained in [60].

7 Conclusions

Summarizing, in this work we study the production of gamma rays in the annihilation of dark matter with a $(1, 0) \oplus (0, 1)$ space time structure. We start noticing that values for the average cross sections of the annihilation into fermions $\langle \sigma v \rangle_f \approx 10^{-26} \text{cm}^3/\text{seg}$ obtained in the fit of the GRE data done in [37], can be obtained for SODM only in the case of resonant processes. Next we perform a systematic study of all the possible mechanisms offered by SODM which produce photonic signals. Mechanisms for prompt photons are classified as initial state radiation, internal bremsstrahlung and final state radiation. We study also delayed photon emission from the inverse Compton scattering of electrons produced directly in the annihilation $\bar{D}D \to e^+e^-$ or secondary electrons from the subsequent decay or hadronization of fermions produced in $\bar{D}D \to ff$ with $f = \mu, \tau, q, c, b$. We find that, for SODM, the main contributions come from the hadronization of $b$ quarks produced in $\bar{D}D \to \bar{b}b$. There are two mechanisms involved: the prompt photons from the hadronization products, and the delayed photon emission in the ICS of electrons produced in the hadronizations process. Similar mechanisms for the $c$ quark, for the $\tau$ lepton decay products and the internal bremsstrahlung, yield sub-leading contributions in the low energy region but become competitive at the end part of the spectrum. All these mechanisms depend only of the SODM mass, $M$, and the scalar Higgs coupling to the SODM, $g_s$. Taking into account all these contributions we find a good agreement with the GRE data for the windows $g_s \in [0.98, 1.01] \times 10^{-3}$ and $M \in [62.470, 62.505] \text{GeV}$.

We check the consistency of these results with the constraints from relic density, direct and indirect detection experiments. Constraints on the dark matter-proton cross section $\sigma_p$ from XENON1T [10] are well satisfied. Our previous calculation of the relic density is based
on the non-relativistic expansion which is broken down by the Higgs resonant effects. We perform a new calculation using the full (relativistic) annihilation cross sections finding substantial modifications near the resonance. The measured relic density [2], turns out to be consistent with the windows for $g_s$ and $M$ imposed by the GRE excess data and correlates these parameters according to figure 10. As for indirect detection experiments, we find consistency with constraints on the annihilation cross section of $\mu^+\mu^-$ [41], $\tau^+\tau^-$ [8] and $\gamma\gamma$ [14, 60]. The consistency with constraints for the annihilation into $b\bar{b}$ [8], requires a detailed bin-by-bin analysis of the energy flux. We find that also in this case our results are consistent with available data.

The results for the annihilation of SODM into $b\bar{b}$ and $\gamma\gamma$ are at the edge of existing upper bounds and lowering these limits would give definite tests of the possibility that dark matter has a $(1,0) \oplus (0,1)$ space time structure and a mass $M \approx M_H/2$, which has been shown here to give a consistent description of the so far calculated observables.

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