Joint Channel Estimation and Signal Recovery in RIS-Assisted Multi-User MISO Communications

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Abstract—Reconfigurable Intelligent Surfaces (RISs) have been recently considered as an energy-efficient solution for future wireless networks. Their dynamic and low-power configuration enables coverage extension, massive connectivity, and low-latency communications. Channel estimation and signal recovery in RIS-based systems are among the most critical technical challenges, due to the large number of unknown variables referring to the RIS unit elements and the transmitted signals. In this paper, we focus on the downlink of a RIS-assisted multi-user Multiple Input Single Output (MISO) communication system and present a joint channel estimation and signal recovery scheme based on the PARAllel FACtor (PARAFAC) decomposition. This decomposition unfolds the cascaded channel model and facilitates signal recovery using the Bilinear Generalized Approximate Message Passing (BiG-AMP) algorithm. The proposed method includes an alternating least squares algorithm to iteratively estimate the equivalent matrix, which consists of the transmitted signals and the channels between the base station and RIS, as well as the channels between the RIS and the multiple users. Our selective simulation results show that the proposed scheme outperforms a benchmark scheme that uses genie-aided information knowledge. We also provide insights on the impact of different RIS parameter settings on the proposed scheme.

Index Terms—Reconfigurable intelligent surfaces, PARAFAC, message passing, MISO, channel estimation, signal recovery.

I. INTRODUCTION

Reconfigurable Intelligent Surfaces (RISs) are lately considered as a candidate technology for beyond fifth Generation (5G) wireless communication due to their potentially significant benefits in low powered, energy-efficient, high-speed, massive-connectivity, and low-latency communications [1]–[9]. In its general form, a RIS is a reconfigurable planar metasurface composed of a large number of hardware-efficient passive reflecting elements [1], [10], [11]. Each unit element can alter the phase of the incoming signal without requiring a dedicated power amplifier, as for example needed in conventional amplify-and forward relaying systems [1], [3], [11].

The energy efficiency potential of RIS in the downlink of outdoor multi-user Multiple Input Single Output (MISO) communications was analyzed in [3], while [12] focused on an indoor scenario to illustrate the potential of RIS-based indoor positioning. It was shown in [13], [14] that the latter potential is large even in the case of RISs with finite resolution unit elements and statistical channel knowledge. Recently, a novel passive beamforming and information transfer technique was proposed in [15] to enhance primary communication, as well as a two-step approach at the receiver to retrieve the information from both the transmitter and RIS. RIS-assisted communication in the millimeter wave [16] and THz [17] bands was also lately investigated. However, the joint channel estimation and signal recovery problem in RIS-assisted systems has not been studied before. Most of the existing research works in RIS-assisted multi-user communications only focus on channel estimation.

The recent works [18] and [19] presented compressive sensing and deep learning approaches for recovering the involved channels and designing the RIS phase matrix. However, the deep learning approaches require extensive training during offline training phases, and the compressive sensing framework assumes that RIS has some active elements, specifically, a fully digital or hybrid analog and digital architecture attached at a RIS portion. The latter architectures increase the RIS hardware complexity and power consumption. A low-power receive radio frequency chain for channel estimation was considered in [5], [20], which also requires additional energy consumption compared to passive RISs. Very recently, [21] and [22] adopted PARAllel FACtor (PARAFAC) decomposition to estimate all involved channels, however, the signal recovery problem was not considered. In addition, some generalized approximate message passing algorithms are proposed for joint estimation and signal recovery, such as bilinear generalized approximate message passing (BiG-AMP) [23], bilinear adaptive generalized vector approximate message passing [24], and generalized sparse Bayesian learning algorithm [25]. In [26], the framework of expectation propagation was employed to perform joint channel estimation and decoding in massive multiple-input multiple-output systems with orthogonal frequency division multiplexing.

In this paper, motivated by the PARAFAC decomposition based channel estimation method [21], [22], we present an efficient joint channel estimation and signal recovery technique for the downlink of RIS-aided multi-user MISO systems. Based on the PARAFAC decomposition, the proposed channel estimation method includes an Alternating Least Squares (ALS) algorithm to iteratively estimate two unknown matrices [27], [28]. With the estimated matrix, the signal and another unknown channel can be estimated simultaneously using BiG-AMP [23]. In such way, we can estimate all involved channels and recover the transmitted signals simultaneously. Represen-
tative simulation results validate the accuracy of the proposed scheme and its superiority over benchmark techniques.

Notation: Fonts $a$, $a$, and $A$ represent scalars, vectors, and matrices, respectively. $A^T$, $A^H$, $A^{-1}$, $A'$, and $\|A\|_F$ denote transpose, Hermitian (conjugate transpose), inverse, pseudo-inverse, and Frobenius norm of $A$, respectively. $a_{mn}$ is the $(m,n)$-th entry of $A$. $|\cdot|$ and $(\cdot)^*$ denote the modulus and conjugation, respectively, while $\circ$ represents the Khatri-Rao matrix product. Finally, notation $\text{diag}(a)$ represents a diagonal matrix with the entries of $a$ on its main diagonal.

II. System and Signal Models

In this section, we first describe the system and signal models for the considered downlink RIS-assisted multi-user MISO communication system, and then present the considered PARAFAC decomposition for the end-to-end wireless communication channel.

A. System Model

We consider the downlink communication between a Base Station (BS) equipped with $M$ antenna elements and $K$ single-antenna mobile users. We assume that this communication is realized via a discrete-element RIS deployed on the facade of a building existing in the vicinity of the BS side, as illustrated in Fig. 1. The RIS is comprised of $N$ unit cells of equal small size, each made from metamaterials capable of adjusting their reflection coefficients. The direct signal path between the BS and the mobile users is neglected due to unfavorable propagation conditions, such as large obstacles. The received discrete-time signals at all $K$ mobile users for $T$ consecutive time slots using the $p$-th RIS phase configuration (out of the $P$ available in total, hence, $p = 1, 2, \ldots, P$) can be compactly expressed with $Y_p \in \mathbb{C}^{K \times T}$ given by

$$Y_p = H^s D_p(\Phi) Y_p X + W_p, \quad (1)$$

where $D_p(\Phi) \triangleq \text{diag}(\Phi_{p,:})$ with $\Phi_{p,:}$ representing the $p$-th row of the $P \times N$ complex-valued matrix $\Phi$. Each row of $\Phi$ includes the phase configurations for the RIS unit elements, which are usually chosen from low resolution discrete sets [13]. $H^s \in \mathbb{C}^{N \times M}$ and $H^r \in \mathbb{C}^{N \times N}$ denote, respectively, the channel matrices between RIS and BS, and between all users and RIS. Additionally, $X \in \mathbb{C}^{M \times T}$ includes the BS transmitted signal within $T$ time slots (it must hold $T \geq M$ for channel estimation), and $W_p \in \mathbb{C}^{K \times T}$ is the Additive White Gaussian Noise (AWGN) matrix having zero mean and unit variance elements.

B. Decomposition of the Received Training Signal

The channel matrices $H^s$ and $H^r$ in (1) are in general unknown and need to be estimated. We hereinafter assume that these matrices have independent and identically distributed complex Gaussian entries; the entries between the matrices are also assumed independent. Our objective in this work is to continuously track $H^s$, $H^r$, and $X$ under the known observation signals $Y$ and few training pilots. To achieve this goal, we propose the following two-stage method. Firstly, we estimate the channel $H'$ and the equivalent matrix $H^e \triangleq H^s X \in \mathbb{C}^{N \times T}$ using in (1) and the PARAFAC decomposition, according to which the intended channels are represented using tensors [29], [30]. Then, the channel $H'$ and the transmitted signal $X$ are simultaneously estimated using the BiG-AMP algorithm [23]. Thus, each $(k,t)$-th entry of $Z_p$, which is the noiseless version of $Y_p$, with $k = 1, 2, \ldots, K$ and $t = 1, 2, \ldots, T$ is obtained as

$$[Z_p]_{kt} = \sum_{n=1}^{N} [H^e]_{kn} [H']_{nt} [\Phi]_{pn}, \quad (2)$$

where $[H^e]_{nt}$, $[H']_{nt}$, and $[\Phi]_{pn}$ denote the $(n,t)$-th entry of $H^e$, the $(k,n)$-th entry of $H'$, and the $(p,n)$-th entry of $\Phi$, respectively, with $n = 1, 2, \ldots, N$.

Resorting to the PARAFAC decomposition [31]–[34], each matrix $Z_p$ in (2) out of the $P$ in total can be represented using three matrix forms. These matrices form the horizontal, lateral, and frontal slices of the tensor composed in (2). The unfolded forms of the mode-1, mode-2, and mode-3 of $Z_p$’s are given in [21] eqs. (6)–(8). In the sequel, we present the proposed joint channel estimation and signal recovery scheme for the simultaneous estimation of the channel matrices $H'$ and $H^e$, and the recovery of the transmitted signals $X$.

III. Propose Joint Channel Estimation and Signal Recovery

The proposed joint channel estimation and signal recovery scheme, which is graphically summarized in Fig. 2, is composed of two main blocks. The first block deals with the estimation of the channels $H'$ and $H^e$. Capitalizing on the latter estimation, the second block simultaneously estimates the channel $H'$ and recovers the transmitted signal $X$. The details of the considered algorithms for these two blocks, as well as the treatment of their possible ambiguities, are presented in following subsections.

A. The First Block

In this block, the ALS-based channel estimation algorithm of [21] is adopted. Specifically, the channels $H'$ and $H^e$ are obtained in an iterative manner by alternatively minimizing conditional Least Square (LS) criteria using the tensor $Y$ for the received signal and the noiseless unfolded forms for all $P$
matrices $Z_p$ (similar to [21], eqs. (6)–(8)). As shown in Fig. 2 (a), two intermediate matrices $A_1 = H^T \circ \Phi$ and $A_2 = \Phi \circ H$ are iteratively updated based on the estimates for $H'$ and $H^c$ at each iteration. At the $i$-th algorithmic iteration, the $i$-th estimation for $H'$, denoted by $\hat{H}'_{(i)}$, is obtained from the minimization of the following LS objective function:

$$ J(\hat{H}'_{(i)}) = \left\| Y_{1} - \tilde{A}_{1}^{(i-1)} (\hat{H}'_{(i)})^T \right\|_F^2, \quad (3) $$

where $\tilde{A}_{1}^{(i-1)} = \hat{H}'_{(i-1)} \circ \Phi$. The solution of (3) is given by

$$ (\hat{H}'_{(i)})^T = (\tilde{A}_{1}^{(i-1)})^T Y_{1}. \quad (4) $$

Similarly, for the $H^c$ estimation, we use the mode-2 unfolded form and formulate the following LS objective function for the $i$-th estimation for $H^c$, which is denoted by $\hat{H}^c_{(i)}$:

$$ J(\hat{H}^c_{(i)}) = \left\| Y_{2} - \tilde{A}_{2}^{(i)} (\hat{H}^c_{(i)})^T \right\|_F^2, \quad (5) $$

where $Y_{2} \in \mathbb{C}^{K_T \times T}$ is the mode-2 matrix-stacked form of tensor $Y$, and $\tilde{A}_{2}^{(i)} = \Phi \circ \hat{H}^c_{(i)}$. The solution of (5) is easily obtained as

$$ \hat{H}^c_{(i)} = (\tilde{A}_{2}^{(i)})^T Y_{2}. \quad (6) $$

The latter estimation method is summarized in Algorithm 1.

**B. The Second Block**

In this block, we jointly estimate $H^c$ and $X$ given the estimated matrix $H^c = H^c X$ and using the BiG-AMP algorithm [23]. First, we derive the following posterior distribution:

$$ p_{X,H^c|H^c}(X, H^c | H^c) = p_{H^c|X,H^c}(H^c | X, H^c) p_{X}(X) p_{H^c}(H^c) \propto p_{H^c|Z}(H^c | H^c X) p_{X}(X) p_{H^c}(H^c) $$

$$ = \left[ \prod_{n=1}^{N} \prod_{t=1}^{T} p_{h_{nt}^a|z_{nt}} \left( h_{nt}^a \right) \sum_{k=1}^{M} h_{nk} x_{kt} \right] \times \left[ \prod_{m=1}^{M} \prod_{t=1}^{T} p_{x_{mt}}(x_{mt}) \right] $$

$$ \times \left[ \prod_{n=1}^{N} \prod_{m=1}^{M} p_{h_{nm}^a}(h_{nm}^a) \right] $$

This joint distribution of $H^c$ and $X$ given $H^c$ can be represented with the factor graph in Fig. 2 (b). In this graph, the factor nodes are represented with white circles. The estimated $H^c$ from the first block is treated as the parameters of the $p_{H^c|Z}$ factor nodes. Applying the BiG-AMP algorithm, the channel $H^c$ and signal $X$ can be estimated, as shown in Algorithm 2.

In Algorithm 2, Steps 3 and 4 compute the ‘plug in’ estimate of $H^c$ and its corresponding variances. Based on this estimate, the Onsager correction is applied in Steps 5 and 6. Afterwards, Steps 7 and 8 calculate the marginal posterior means and variances, respectively, of $H^c$. Considering that $H^c$ is the output of the first stage (i.e., the output of Algorithm 1), we assume the noise to be zero, thus the scaled residual and corresponding variances are computed in Steps 9 and 10 without the AWGN term. In the sequel, steps 11 and 12 compute the means and variances of the corrupted version of the estimation for $X$, and then, Steps 13 and 14 calculate the
means and variances of the AWGN-corrupted observation of the estimated channel $H^\ast$. Finally, based on the priors of $X$ and $H^s$, the posteriors of $X$ and $H^s$ are computed in Steps 15 until 18, as follows:

$$P_{\hat{r}_mt|x_m}(x_m | \hat{r}_mt(i); \nu^s_{mt}(i))$$

and

$$P_{rmt|x_m}(x_m | \hat{r}_mt(i); \nu^s_{mt}(i)) = N(\hat{r}_mt(i); x_m, \nu^s_{mt}(i))$$

The latter model is assumed in each $i$-th iteration of the BiG-AMP algorithm. Similarly, the posterior probability (9) is used to compute the variances and means of $x_m, \forall m$ in Steps 15 and 16. In fact, the probability (8) can be interpreted as the exact posterior probability of each $x_m$ given the observation $r_{mt}$ under the prior model $P_{x_m}(x_m)$ and the likelihood model $P_{rmt|x_m}(\hat{r}_mt(i) | x_m; \nu^s_{mt}(i)) = N(\hat{r}_mt(i); x_m, \nu^s_{mt}(i))$. The latter model is assumed in each $i$-th iteration of the BiG-AMP algorithm. Similarly, the posterior probability (9) is used to compute the variances and means of $h^s_{nm}$ under the prior model $p_{h^s_{nm}}(h^s_{nm})$ and the likelihood model $p_{qnm|h^s_{nm}}(qnm(i) | h^s_{nm}; \nu^q_{nm}(i)) = N(\hat{q}_nm(i); h^s_{nm}, \nu^q_{nm}(i))$.

C. Ambiguity Removing

The proposed joint estimation and signal recovery scheme involves ambiguities in the two blocks in Fig. 2. In the first block, the iterative estimation of $H^s$ and $H^h$, using the ALS approach included in Algorithm 1, encounters a scaling ambiguity from the convergence point, which can be resolved with adequate normalization [30], [35]. To tackle this issue, the first column of $H^s$ has been normalized.

In the second block, phase and scaling ambiguities exist in the estimation of $H^s$ and $X$ using Algorithm 2. To remove the latter ambiguity, we assume initial pilot signal transmission in $X$. For the phase ambiguity, we adopt the method in [36]. In particular, the transmitted signal is designed to be a full-rank matrix. It is generated from the Bernoulli Gaussian distribution with sparsity $\beta$ ($\beta$ is the portion of nonzero elements in transmitted signal), and sparsity pattern known to the receivers. With the latter settings, the ambiguities can be removed from the proposed scheme.

D. Computational complexity

In Algorithm 1, the computational complexities for the estimations of $H^s$ and $H^h$ are $O(N^3 + 4N^2KP - NK + 2NMKP - NM)$ and $O(N^3 + 4N^2MP - NMP + 2NMKP - NK)$, respectively. Thus, using the feasibility condition in the proposed PARAFAC-based structure [21], the total computational complexity for this algorithm becomes $O(N^3 + 4N^2MKP)$. The complexity of Algorithm 2 is dominated by the matrix multiplications per algorithmic iteration. In Steps 3 up to 5, as well as from Steps 11 until 14, each computation requires $NM$ multiplications, where the computations within Steps 6 and 10 are of the order $O(NM + MT)$. Thus, Algorithm 2 requires $O(NMT + NM + MT)$ mathematical operations per iteration. Putting all above together, the total computational complexity of the proposed joint channel estimation and signal recovery scheme is $O(2N^3 + 4NMKP + NMT + NM + MT)$. 

Algorithm 2 The Bi-GAMP Algorithm [23]

Input: $H^s$, $\epsilon > 0$, and the number of maximum algorithmic iterations $I_{max}$.

1: Initialization: Initialize $\hat{r}_{mt}(0) = 0$, and choose $\nu_{mt}(0), \nu_{nm}(0), \tilde{h}^s_{nm}(1), n = 1, \ldots, N, t = 1, \ldots, T, m = 1, \ldots, M$.

2: for $i = 1, 2, \ldots, I_{max}$ do

3: \forall n, t : $\tilde{p}^s_{nt}(i) = \sum_{n=1}^{N} \tilde{h}^s_{nm}(i)^2 \nu^s_{mt}(i) + \nu^s_{nm}(i) | \tilde{r}_{nt}(i)$

4: $\forall n, t : \nu^s_{nt}(i) = \nu^s_{nt}(i) + \sum_{n=1}^{N} \nu^s_{nm}(i) \nu^s_{mt}(i)$

5: $\forall n, t : \tilde{p}^s_{nt}(i) = \tilde{p}^s_{nt}(i) - \tilde{s}_{nt}(i - 1)$

6: $\forall n, t : \nu^s_{nt}(i) = \nu^s_{nt}(i) + \sum_{n=1}^{N} \nu^s_{nm}(i)$

7: $\forall n, t : \nu^s_{nt}(i) = \nu^s_{nt}(i) - \tilde{s}_{nt}(i)$

8: $\forall n, t : \tilde{r}_{mt}(i) = \tilde{r}_{mt}(i) - \nu^s_{nt}(i)$

9: $\forall n, t : \nu^s_{nt}(i) = \nu^s_{nt}(i) - \nu^s_{nt}(i)$

10: $\forall n, t : \tilde{r}_{mt}(i) = \tilde{r}_{mt}(i) - \nu^s_{nt}(i)$

11: $\forall n, t : \tilde{r}_{mt}(i) = \tilde{r}_{mt}(i) - \nu^s_{nt}(i)$

12: $\forall n, t : \tilde{r}_{mt}(i) = \tilde{r}_{mt}(i) - \nu^s_{nt}(i)$

13: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

14: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

15: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

16: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

17: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

18: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

19: $\forall n, m : \tilde{r}_{nt}(i) = \tilde{r}_{nt}(i) - \nu^s_{nt}(i)$

20: end for

Output: $\tilde{h}^s_{nm}$ and $\tilde{X}_{mt} = \tilde{x}_{mt}$, respectively.

IV. PERFORMANCE EVALUATION RESULTS

In this section, we present computer simulation results for the performance evaluation of the proposed joint channel estimation and signal recovery scheme. We have particularly simulated the Normalized Mean Squared Error (NMSE) of the proposed scheme using the metrics $\|H^s - H^s\|^2$, $\|H^h - H^h\|^2$, $\|H^s - H^h\|^2$, and $\|X - \tilde{X}\|^2$. The scaling ambiguity in our two-stage estimation has been removed by normalizing the first column of $H^s$, such that it has all one elements. For $\Phi$, we have considered the discrete Fourier transform matrix, which satisfies $\Phi^H \Phi = \mathbf{I}_N$ and has been suggested as a good choice for ALS [30]. All NMSE curves were obtained after averaging over 500 independent Monte
It is shown that there exists a tradeoff between the NMSE scheme is investigated in Fig. β increase, which result in performance loss. The impact of the those cases, the numbers of unknown variables for estimation exists an increasing performance loss when M scheme as a function of the SNR. It is evident that there M of N = 32 X be found in [21]. In addition, the illustrated abnormality in the parameter setting. More details for solely the channel estimation methods: i) LS Khatri-Rao factorization (LSKRF) [22]; and ii) conventional LS estimation, for the estimation part in the benchmark schemes. In Fig. 3 using the setting K = 32, N = 16, M = 12, N = 16, T = 100, P = 16, and β = 0.2, it is shown that proposed scheme achieves similar performance with the one that adopts LSKRF estimation. However, our scheme is more robust to parameter setting changes compared to the one with LSKRF estimation. As depicted in Fig. 4 the parameter setting is changed to K = 32, N = 20, M = 12, N = 16, T = 100, P = 16, and β = 0.2. It is observed that the estimation performance of the LSKRF scheme gets dramatically deteriorated with slight changes of N, witnessing its increased sensitivity in the parameter setting. More details for solely the channel estimation comparison between our scheme and LSKRF can be found in [21]. In addition, the illustrated abnormality in the estimation of the signal X happens due to its high sparsity and pilots. It is shown in Figs. 3 and 4 that the proposed scheme has only about 2.5dB performance gap from the LS scheme that assumes perfect channel knowledge. This behavior substantiates the robustness and favorable performance of our proposed scheme.

In Fig. 5 we have used the simulation parameters K = 16, N = 32, T = 100, P = 16, β = 0.2, and various values of M to illustrate the NMSE performance of the proposed scheme as a function of the SNR. It is evident that there exists an increasing performance loss when M increases. In those cases, the numbers of unknown variables for estimation increase, which result in performance loss. The impact of the sparsity level β in the NMSE performance of the proposed scheme is investigated in Fig. 6 as a function of the SNR for K = 20, N = 32, M = 16, T = 100, and P = 16. It is shown that there exists a tradeoff between the NMSE performance and β. The scheme for β = 0.5 suffers the worst performance. This happens because more non-zero variables need to be estimated with increasing β, which makes the BiG-AMP algorithm to performs worse. It can be also seen that the performance for β = 0.1 is worse than for β = 0.3 (of around 3dB), even that less unknown variables are involved. This behavior accounts for the possible sparsity pattern collision. Actually, when multiple users are located close to each other, recovery failures happen [37].

V. CONCLUSION

In this paper, we presented a joint channel estimation and signal recovery scheme for RIS-assisted multi-user MISO communication systems, which capitalizes on the PARAFAC decomposition of the received signal model. All involved channels are estimated and the transmitted signal is recovered using a two-stage approach. In the first stage, the channel between RIS and the users and another equivalent channel are estimated using ALS. Then, in the second stage using the equivalent channel estimation, the channel between the BS and RIS and the transmitted signals are recovered via the BiG-AMP algorithm. Our simulation results showcased that the proposed joint channel estimation and signal recovery scheme

Figure 3. NMSE performance comparisons between the proposed algorithm, LSKRF [22], and genie-aided LS estimation versus the SNR in dB for K = 32, N = 16, M = 12, N = 16, T = 100, P = 16, and β = 0.2.

Figure 4. NMSE performance comparisons between the proposed algorithm, LSKRF [22], and genie-aided LS estimation versus the SNR in dB for K = 32, N = 20, M = 12, N = 16, T = 100, P = 16, and β = 0.2.

Figure 5. NMSE performance of the proposed algorithm versus the SNR in dB for K = 16, N = 32, T = 100, P = 16, β = 0.2, and various values M for the BS antennas.
outperforms various benchmarks. In addition, we observed that the number of BS antennas $M$ and the sparsity level $\beta$ exert a significant effect on our proposed algorithm.

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