Hawaii Two-0: High-redshift galaxy clustering and bias

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1 INTRODUCTION

The standard Lambda cold dark matter (ΛCDM) cosmological model has proven extremely successful in describing various observations of the Universe. The main observational pillars of this model have been the cosmic microwave background (CMB) at redshift \( z \approx 1100 \), type Ia supernovae up to around \( z \approx 1 \), and the large-scale structure in various wide-angle galaxy surveys (e.g., SDSS/BOSS, Dawson et al. 2013; Pan-STARRS, Chambers et al. 2016; DES, Dark Energy Survey Collaboration et al. 2016), with depths reaching up to \( z \approx 1.5 \). Quasar maps are deeper (e.g., Gil-Marín et al. 2018, up to \( z \approx 2.2 \)), at the expense of being restricted to the largest scales due to shot noise.

Thus, despite enormous progress in pushing the limits of depth, currently there are few measurements available to anchor the ΛCDM model in the redshift range between the CMB and the deepest wide-angle surveys. In the future, LSST will extend to \( z \approx 3–4 \) and will cover an area of 30,000 square degrees (Ivezic et al. 2008), while Euclid (Laureijs et al. 2011) and WFIRST (Akeson et al. 2019) will reach \( z \approx 2, 3 \), respectively, the latter in a smaller footprint.

The Hawaii Two-0 (H20) survey fills the redshift gap in observations — it is a 20 square degree ultra-deep optical galaxy survey with gri\textsuperscript{y} broad-band photometry from the Hyper-Suprime Cam (HSC) instrument of the Subaru telescope. It has two fields of 10 square degrees each, at the North Ecliptic Pole and Chandra Deep Field-South. The former overlaps with the Euclid Deep Calibration Field, thus enabling synergy between observations. The expected depths in each band for H20 are shown in Table 1.

Hawaii Two-0 will include broad-band measurements of galaxies up to \( z \approx 7 \). At this redshift, the comoving distance across each 10 square degree field is roughly 500 Mpc, large enough to include several clusters. This coverage facilitates studying galaxy evolution as it relates to environment at an unprecedented depth, while also providing a sample large enough for cosmological study. In fact, the total volume of H20 out to \( z = 7 \) will be roughly 1.4 Gpc\textsuperscript{3}.

The most elementary parameter to characterize a galaxy sample is the linear galaxy bias \( b_{\text{gal}} \). This connects the theoretically modelled matter overdensity \( \delta \) to the measured galaxy overdensity \( \delta_{\text{gal}} \): \( \delta_{\text{gal}} = b_{\text{gal}} \delta \). More precisely, \( b^2 \)
Table 1. Top: observational parameters for the Hawaii Two-0 survey — 5-sigma point source limiting magnitudes, HSC exposure times. Bottom: 5-sigma point source limiting magnitudes for the SSP + UH HSC stack (Tanaka et al. 2017), used in this paper.

| Filter                  | $g$  | $r$  | $i$  | $z$  | $y$  |
|-------------------------|------|------|------|------|------|
| H20 limiting mag        | 27.5 | 27.5 | 27.0 | 26.5 | 26.0 |
| H20 exposure time       | 1.1h | 2.5h | 4.1h | 4.8h | 9h   |
| SSP+UH limiting mag     | 27.8 | 27.7 | 27.6 | 26.8 | 26.2 |

is the ratio of galaxy and dark matter power spectra under the assumption that a deterministic and linear bias holds. This is expected to be true on the large scales we consider in this paper.

While the galaxy bias is sample-dependent and difficult to interpret on its own, it is a necessary stepping stone towards more universal cosmological parameters. In particular, the amplitude of fluctuations, often described with the parameter $\sigma_8$, is entirely degenerate with $b_{\text{gal}}$ from two-point clustering measurements.

Recent work (e.g., McCarthy et al. 2018) reveals a mild tension between the concordance value of $\sigma_8$ within $\Lambda$CDM cosmology and measurements of clustering in the local universe. A high-redshift constraint on $\sigma_8$ would help decide the significance of this tension.

Since H20 observations are ongoing, we chose to perform an analysis of galaxy bias on a readily available HSC data set, allowing us to test our methodology and software in preparation for the processing of actual H20 data.

Sect. 2 describes our data sets, Sect. 3 outlines the theoretical background, Sect. 4 details our methods to extract the redshift distribution of our samples, Sect. 5 describes the angular power spectra obtained and the linear galaxy bias fits, and finally Sect. 6 summarizes and discusses our results. Appendix A contains an analysis of the magnification bias that is ancillary to our main topic.

2 DATA SET

2.1 Photometric data

An earlier HSC survey, performed jointly by the Subaru Strategic Program and the University of Hawaii, provides ultra-deep optical images in the COSMOS field (SSP+UH survey, Tanaka et al. 2017). The data set is public, uses the same instrumentation as H20, and has a similar — albeit slightly higher — depth. Table 1 lists the limiting magnitudes of SSP+UH in each photometric band, as well as the anticipated corresponding values for H20. While the SSP+UH survey has full depth in only one HSC pointing (with an area of $\approx 1.8$ square degrees), it was selected as the best candidate to perform our preliminary analysis for H20.

In this work, we use the reduced data and source catalogue of Tanaka et al. (2017), specifically the fluxes measured in a 1.5$''$ diameter circular aperture, in the HSC $grizy$ broad-band photometric filters.

2.2 Dropout selection

To select galaxy sub-samples within a well-defined redshift range, we adopt the methodology of the GOLDRUSH project of the Subaru Strategic Program (Ono et al. 2018; Harikane et al. 2018). Following Hildebrandt et al. (2009), they defined colour cuts and measurement quality criteria in order to select dropout samples in the HSC $g$, $r$, $i$, and $z$ bands, which they found to correspond to redshift bins around $z \approx 4$, $z \approx 5$, $z \approx 6$ and $z \approx 7$, respectively, with little overlap.

We consider only the $g$-, $r$-, and $i$-band dropouts, since $z$-band dropouts by definition are detected in the $g$-band only and thus have a higher risk of including spurious detections. The original colour cuts for our three dropout bands were defined in Ono et al. (2018) as

$$g - r > 1.0$$

$$r - i < 1.0$$

for $g$-dropouts,

$$i - z < 0.7$$

$$z - y < 0.5$$

$$i - z > 2.0(z - y) + 1.1$$

for $i$-band dropouts.

Additionally, Ono et al. (2018) required that $g$-dropouts have signal-to-noise ratio $S/N > 5.0$ in $i$-band, $r$-dropouts have $S/N > 5.0$ in $z$-band, and $i$-dropouts have both $S/N > 5.0$ in $z$-band and $S/N > 4.0$ in $y$-band. Finally, $r$-dropouts had to be undetected (specifically, $S/N < 2.0$) in $g$-band, and $i$-dropouts needed to be undetected in both $g$- and $r$-bands. We adopt these criteria as well.

The equations above reveal that $g$-dropouts require photometry in the $g$-, $r$-, and $i$-bands, $r$-dropouts in the $r$-, $i$-, and $z$-bands, and finally $i$-dropouts in the $i$-, $z$-, and $y$-bands. Sources that have valid photometry and are not flagged for any artifacts (e.g., satellite trail, saturation, diffraction spike; Ono et al. 2018) in these three sets of photometric bands constitute the parent catalogs from which the respective dropout samples are selected. The pixels in the field that have valid photometry, and have not been flagged for any issue are shown in Fig. 1.

We also performed an independent test of the validity of the colour cuts using the combined spectroscopic catalog in the COSMOS field (M. Salvato, private communication). The well-measured spectroscopic sources (quality flag $Q > 3$) were cross-matched with the three dropout samples using a matching radius of 1.5$''$. We found 750, 63 and 2 spectroscopic matches with the $g$-, $r$- and $i$-dropouts, respectively.

Tests done by Ono et al. (2018), using both template spectra and spectroscopic galaxies from VVDS, noticed no significant low-redshift contamination in their ultra-deep COSMOS sample, which is most similar to our data set.
Contrary to this however, we found that 75.3% of the g-band matches were below \( z = 3 \), with most contaminants having \( z < 1 \). The left panel of Fig. 2 shows the position of these contaminants in colour space, along with the colour cut. Clearly, the low-redshift galaxies are scattered around the original cut boundary; therefore we decided to raise the diagonal boundary by 0.4 mag, and thus the empirical colour cut we use for g-band dropouts became

\[
\begin{align*}
&g - r > 1.0 \\
r - i < 1.0 \\
g - r > 1.5(r - i) + 1.2,
\end{align*}
\]

instead of Eq. 1.

While the new colour cut reduces the size of the g-band dropout sample by 49.0%, \( z < 3 \) contaminants in the matched sample were limited to only 11.6% (13 out of 112 remaining matches). We note that the spectroscopic sample we matched with is not at all representative of the photometric dropout samples in terms of the distribution of observables and underlying physical parameters, due to significant biases introduced by the target selection. In fact, the spectroscopic sample is extremely biased towards low-redshift sources, as illustrated on the right panel of Fig. 2. Because of this, we can assume that the level of contamination in the dropout sample does not exceed a few percent with the updated cut.

A similar analysis of \( r \)- and \( i \)-band dropouts provided no evidence of such issues, albeit the sample size was very limited: 3 of 63 matches had \( z < 4 \) for the \( r \)-dropouts, and neither of the 2 \( i \)-band matches were below \( z = 5 \). Thus, in these bands the cuts were left unchanged.

The disparity between our findings and those of Ono et al. (2018) regarding g-band dropout selection in the ultra-deep field is potentially attributable to the spectroscopic targeting of VVDS, or a difference in photometric scatter.

A more thorough analysis of this issue is left to a future work.

After applying the colour and quality cuts to the SSP+UH catalog, we obtain 36769, 3815 and 262 galaxies in the \( g \)-, \( r \)- and \( i \)-band dropout samples, respectively. The top row of Fig. 3 shows the position of these galaxies in the sky.

3 THEORY

In this section, we briefly present the theoretical calculations performed while deriving the linear galaxy bias. (See Desjacques, Jeong & Schmidt 2018 for a comprehensive review of galaxy bias.) Our specific notation follows Beck et al. (2018) and was influenced by the equations in Peiris & Spergel (2000); Afshordi (2004); Ho et al. (2008); Loverde, Hui & Gaztañaga (2008); Ziou & Hui (2008).

Typically, a galaxy survey measures the \( n_{\text{gal}}(\theta) \) projected number count of sources in a given \( \theta \) direction on the sky. This quantity converts to galaxy overdensity as

\[
\delta_{\text{gal}}(\theta) = \frac{n_{\text{gal}}(\theta) - \pi_{\text{gal}}(\theta)}{\pi_{\text{gal}}(\theta)},
\]

where \( \pi_{\text{gal}}(\theta) \) is the mean number count.

The linear galaxy bias \( b_{\text{gal}} \) is defined through the relation \( \delta_{\text{gal}} = b_{\text{gal}} \delta \), which assumes a simple linear relationship between the underlying matter distribution and that of the matter tracers, i.e. the galaxies. Thus, a computation of the theoretical expectation for the overall matter overdensity \( \delta \) is required to find \( b_{\text{gal}} \).

There are several public cosmology codes that can compute the theoretical \( P_3(k,z) \) power spectrum of the matter overdensity via a Boltzmann equation framework, e.g., CMBFAST (Seljak & Zaldarriaga 1996), CAMB (Lewis, Challinor & Lasenby 2000; Lewis & Challinor 2002; Challinor & Lewis 2005) and CLASS (Lesgourgues 2011). \( P_3(k,z) \) is the power spectrum of \( \delta(k,z) \), the Fourier transform of the 3D overdensity field, which we wish to relate to the angular \( \delta_{\text{gal}}(\theta) \) that we measure.

Given the redshift distribution \( \Pi(z) = dN_{\text{gal}}/dz \) of the tracer sample, and the redshift-dependent linear bias \( b(z) \), we can perform a spherical projection through the expression

\[
C^\text{gal}_l^{\Pi} = \frac{2}{\pi} \int dk \frac{k^2}{(2l+1)} \left[ G_l^3(k) \right]^2 + C_{\text{Poisson}},
\]

where we have the kernel function for galaxy density

\[
G_l^3(k) = \int d\tau \frac{b(z(\tau))}{r_j(z(\tau))} \frac{d^2 P_3(k,z(\tau))}{dz^2} j_l[\chi(\tau)k],
\]

and the constant Poisson shot noise term

\[
C_{\text{Poisson}} = \frac{4\pi f_{\text{sky}}}{N_{\text{gal}}},
\]

In Eqs. 7-8, \( \tau \) denotes the conformal time, \( \chi(\tau) = c(\tau_0 - \tau) \) is the conformal lookback distance, \( j_l \) is a spherical Bessel function of the first kind, \( f_{\text{sky}} \) represents the sky coverage fraction of the survey, and \( N_{\text{gal}} \) is the number of density of tracer objects (i.e. galaxies). We define \( P_3(k,z) = \sqrt{P_3^g(k,z)} \). Also, \( \Pi(z) \) is normalized to unit integral.

The \( C_{\text{Poisson}} \) term has been added to account for the fact that, in practice, a survey measures a discrete number count...
of objects in a given sky pixel, which is affected by Poisson shot noise. The autocorrelation of this noise component is positive and does not depend on the $l$ spherical index.

In the literature, the assumption of linear growth is often made, introducing the $D(z(\tau))$ growth factor to describe the redshift dependence of the matter power spectrum, yielding the expression $P_3(k, z) = D^2(z(\tau))P_0(k)$. This way, $P_0(k)$ can be moved outside $[G_k^g(k)]$ in Eq. 6 to speed up the calculation. We do not make this assumption in our work.

When dealing with small angular scales (e.g., $l > 20$), the Limber approximation (Limber 1953; Kaiser 1992) is often adopted to considerably reduce computational cost by simplifying the Bessel functions. Since our survey area is rather small, we can safely make this assumption. Under the Limber approximation, Eq. 6 becomes

$$C_{l}^{gg} = \int d\tau \frac{1}{c\chi^2(\tau)}P_3(k, z(\tau))b^2(z(\tau))\Pi^2(z)\left(\frac{dz}{d\tau}\right)^2 + 4\pi f_k\frac{\nu_s}{N_{gal}}.$$  

Instead of using the general, redshift-dependent form for the linear galaxy bias, we assume and fit a single bias value for each dropout band, therefore $b(z(\tau)) = b_{gal}$.

$C_{l}^{gg}$ is the theoretical spherical autocorrelation power spectrum of the galaxy overdensity, and it scales with $b^2$. By measuring the $\delta_{gal}(\theta)$ overdensity map in our survey, and computing its autocorrelation, we get $C_{l}^{gg}$, the empirical spherical power spectrum. We can then simply fit $b$ by scaling $C_{l}^{gg}$ to $C_{l}^{gg}$.

We note that in magnitude-limited samples, gravitational lensing magnification by foreground matter can provide a contribution to the observed $\delta_{gal}(\theta)$ overdensity. We show in Appendix A that such magnification bias is negligible in our data set.

We use PolSpice (Szapudi et al. 2001; Challinor et al. 2011) to calculate empirical spherical power spectra, as it can handle heavily masked fields. Also, we use PyCAMB1, a Python wrapper for CAMB, to compute $P_3(k, z)$. We have developed the SPHERICOSMO2 Python package both to wrap the required functionality in PolSpice and PyCAMB, and to compute, in a convenient manner, the Bessel and Limber spherical power formulas for matter, the integrated Sachs-Wolfe effect, and the auto- and cross-correlations for weak lensing and lensing magnification.

For all calculations in this paper, we adopted the cosmological parameters of Planck Collaboration (2016), specifically the following: $H_0 = 67.74$, $\Omega_m h^2 = 0.2223$, $\Omega_k h^2 = 0.1188$, $\tau = 0.066$, $n_s = 0.9667$, $\sigma_8 = 0.8159$, spatially flat geometry, and no contribution from tensor modes (i.e. $\Omega_k = 0$ and $\tau_{0.02} = 0$). Additionally, a single massive neutrino of mass $m_{\nu} = 0.06\,\text{eV}$ was assumed.

4 REDSHIFT DISTRIBUTIONS

As discussed in Sect. 3, the $\Pi(z)$ redshift distribution of the matter tracer sample is required to compute Eq. 9. Thus, we need to estimate the redshift distribution of the $g$-band, $r$-band, and $i$-band dropout galaxy samples.

To perform this task, we turn to photometric redshift (photo-z) estimation. A wide variety of methods have been published in the literature, which can broadly be categorized as either machine learning (Csabai et al. 2003; Wadadekar

1 http://camb.readthedocs.io/en/latest/
2 https://github.com/beckrob/Sphericosmo
2005; Carliles et al. 2010; Gerdes et al. 2010; Brosca et al. 2014; Beck et al. 2016) or spectral template fitting (Benítez 2000; Arnouts et al. 2002; Coe et al. 2006; Ilbert et al. 2006; Brammer, van Dokkum & Coppi 2008; Beck et al. 2017a) approaches. Refer to Hildebrandt et al. (2010); Dahlen et al. (2013); Beck et al. (2017b) for comparisons of different methods.

At the high redshifts which we are probing, the spectroscopic coverage is very limited. Thus, machine learning photo-z methods are effectively ruled out, as they rely on a spectroscopic training set that should cover the space of physical parameters. Instead, we selected EAZY\textsuperscript{3}, a public template fitting photo-z code (Brammer, van Dokkum & Coppi 2008; Brammer et al. 2011) to perform the redshift estimation.

We ran EAZY in two configurations, the first with the default set of spectral templates and settings, denoted by EAZY-def, and the second using the updated templates of the newest code release, denoted by EAZY-new. The redshift grid spanned $z = 0.001 - 8.0$ with a step size of $0.01/(1 + z)$. We use the $z_{\text{peak}}$ maximum likelihood redshift output.

\textsuperscript{3} https://github.com/gbrammer/eazy-photoz

4.1 Monte Carlo sampling

The $r$- and $i$-dropout samples are relatively small in size (3815 and 262 galaxies), which means that, taken directly, their redshift histograms would be a rather crude sampling of the underlying $\Pi(z)$ distribution. One option would be to simply smooth the histograms by the estimated redshift inaccuracy; however, that would artificially blur the sharp boundaries expected in such dropout samples (Ono et al. 2018).

We chose to instead perform a Monte Carlo sampling of the colour space, randomly generating fluxes for each source by sampling from Gaussian distributions with the same mean and standard deviation as each measured flux and flux error. Photometric errors are a major obstacle in obtaining accurate photo-z-s, as they enhance degeneracies between different galaxy types at different redshifts (Benítez 2000). By augmenting our galaxy samples in this manner, our goal is to better represent their colour space footprint, and at the same time take into account photometric errors in the photo-zs without arbitrarily modifying the redshift distribution itself.

In practice, we performed the Monte Carlo flux sampling on the parent catalog of each dropout sample, and
only afterwards applied the dropout colour and quality cuts (see Sect. 2.2). This was done to simulate galaxies randomly scattering across the colour cut boundaries. Over 5 million samples were generated for each dropout band to ensure the colour space is properly covered, and the results are stable.

4.2 Self-organizing maps

As spectral template fitting photo-z approaches are comparatively slow, we followed the approach of Masters et al. (2015, 2019) and used self-organizing maps (SOMs) to quantize the large number of Monte Carlo samples into a much smaller number of colour space cells. We trained SOMs on the parent catalog of each dropout sample and projected from the 5D magnitude space into a two-dimensional 100 × 100 rectangular grid of SOM cells. To perform this computation, we used the SOMPY\(^4\) Python package.

The SOM introduces another source of randomness into the results, as the training process involves random starting points for the cells, and the training data is also processed in random order. To ensure the stability of the results, we trained 20 different SOMs for each dropout sample, and the final redshift distributions have been averaged over these instances.

4.3 Redshift results

With the SOM projection done, we only need to run EAZY on the centrepoint of each SOM cell (in 5D magnitude space, converted to fluxes), and then the photo-z of each cell is weighted by the number of Monte Carlo samples that fell into that cell when creating the redshift histogram.

As described above, the whole process, including the random sampling, has been repeated for 20 SOM instances, and the SOM-wise redshift histograms have been averaged for every redshift bin.

The resulting final redshift histograms for the EAZY-def and EAZY-new configurations, for the three dropout galaxy samples, are shown in Fig. 4. For reference, we also show the redshift histograms from Ono et al. (2018) for their similar dropout samples. While the histograms for a given dropout band are largely similar, it is clear that the choice of templates (and, more broadly, methodology) can lead to significant redshift bias and change in the shape of the histograms.

Furthermore, despite the random sampling, the peculiarities of a template set can lead to relatively sharp peaks. Based on our tests of the dropout cuts in Sect. 2.2, and on the fact that the peaks change both shape and position with the choice of templates, we do not believe the sharp peaks are physical. For this reason, we introduce a small amount of smoothing to the two sets of histograms, using a Gaussian kernel of \(\sigma = 0.01/(1 + z)\). The smoothed redshift histograms, denoted EAZY-def-sm and EAZY-new-sm, are also shown in Fig. 4.

5 GALAXY AUTOCORRELATION RESULTS

We next computed \(\delta_{gal}(\theta)\) for HealPix\(^5\) (Górski et al. 2005) pixelized maps of the \(g\)-, \(r\)- and \(i\)-band dropout galaxy samples, shown in the bottom row of Fig. 3. Specifically, we used the HealPy\(^6\) Python wrapper, choosing a HealPix resolution of NSIDE = 1024.

We note that the HealPix pixels in Fig. 3 are \(\approx 3600\) times larger in area than the original pixels of the detection mask in Fig. 1. We consider HealPix pixels with less than a 40% valid detection area as masked, and within non-masked pixels the object counts were weighted in accordance with their valid area to calculate the overdensity.

\(^4\) https://github.com/sevamoo/SOMPY

\(^5\) http://healpix.sourceforge.net/

\(^6\) https://github.com/healpy/healpy
We then utilized the PolSpice package (via SPHERICOSMO, see Sect. 3) to compute the $C_{l}^{gg}$ empirical spherical autocorrelation power spectra of the three overdensity maps. Because of the small survey area of SSP+UH, apodization of $\theta = 1.374^\circ$ was required to ensure numerical stability (Szapudi, Prunet & Colombi 2001; Szapudi et al. 2005).

Our HealPix resolution choice of NSIDE = 1024 allows us to safely perform an analysis up to a spherical index of $l \simeq 2000$. At higher values of $l$, the scales are small enough that, even at the high redshift of our samples, the non-linear component of the matter power spectrum would start to dominate. As the modelling of the matter power spectrum is more complex in non-linear regime, we terminated our analysis at $l_{\text{max}} = 2000$.

To obtain the minimum $l$, corresponding to the largest scales we can probe, the obvious limitation is the small area of the survey. An angular separation of $1^\circ$ roughly corresponds to $l \simeq 180$, and therefore we selected $l_{\text{min}} = 200$ as the largest scale such that enough galaxy pairs exist in the two-point correlation.

A side effect of the apodization performed by PolSpice is that nearby $l$ values in the power spectrum become correlated and thus can no longer be considered independent measurements. To account for this fact, we bin $C_{l}^{gg}$ into $l$-bands of width $\Delta l = 300$, weighting each $l$ uniformly, and computing the error of the binned measurement from the block-average of the covariance matrix reported by PolSpice.

In summary, our analysis focuses on 6 $l$-bands of width 300, covering the range $l = 200 - 2000$. The raw and binned autocorrelation power spectra appear in Fig. 5.

In addition to $C_{l}^{gg}$, we determined the $C_{l}^{gg}$ theoretical autocorrelation power spectra using Eq. 9, as implemented in Sphericosmo. We calculated the spectra for each of the four redshift distributions described in Sect. 4.3: EAZY-def, EAZY-def-sm, EAZY-new and EAZY-new-sm. Additionally, for reference, we performed the computations for the Ono et al. (2018) redshift distributions, labelled Ono2018. The theoretical spectra were binned in the same way as the empirical spectra.

Finally, for each redshift setup, the best-fitting $b_{\text{gal}}$ linear bias was computed using the Levenberg-Marquardt method (see chapter 15.5.2 of Press et al. 2007, as implemented by the curve_fit function of SciPy), fitting the binned $C_{l}^{gg}$ values to the binned $C_{l}^{gg}$ values.

We show the bias fit results for all redshift setups in Fig. 6. Theoretical curves corresponding to both the non-linear (which uses a halo model) and linear 3D matter power spectra from CAMB are plotted, but we report the results only for the non-linear model. The autocorrelation curve shapes of the different models are barely different, except for their amplitude, and thus the fitted $b_{\text{gal}}$. One discernible disparity is the amount of extra power the non-linear model predicts, especially at high $l$ values for the EAZY-new configuration and the $g$-band dropouts. The non-linear, small scales are mainly introduced by the sharp $z \simeq 0.4$ peak of the redshift histogram, as predicted by the photo-$z$ method (see Fig. 4). Without a spectroscopic sample which is representative of our dropout catalogs, we currently have no reasonable method of better constraining the relative strength of these low-$z$ contaminant peaks.

The fitted $b_{\text{gal}}$ values of Fig. 6 demonstrate that the particular choices made when deriving the $\Pi(z)$ distributions can significantly affect the results. In fact, the systematic bias caused by the $\Pi(z)$ setup is as large as, or even larger than the statistical uncertainty of the measurements, even with the relatively small sample sizes available in the SSP+UH survey.

We attempt to quantify the systematic bias in our results by artificially adding plausible amounts of photo-$z$ bias to our most reasonable photo-$z$ configuration.

5.1 Systematic effects of photo-$z$ bias

The EAZY-new-sm photo-$z$ setup has been chosen as our fiducial $\Pi(z)$ distribution in the following test, for several reasons. First, it yielded the median of the five $b_{\text{gal}}$ values in our fits for the $i$-band and $r$-band dropouts (and was one away from the median for $g$-dropouts). Second, it utilizes the newest, most complete set of template spectra available with EAZY. Third, while the distribution shows some unphysical “peakiness”, it has been somewhat mitigated by the applied extra smoothing.

Figure 5. Empirical spherical autocorrelation power spectra for the $g$-, $r$- and $i$-band dropout galaxy samples, from left to right. Dotted lines show the raw measured spectra, while points and error bars represent the binned measurements and their uncertainty. The black dashed line depicts the expected $C_{l}^{\text{Poisson}}$ shot noise.
Starting with this fiducial distribution, we applied an artificial redshift bias of $\Delta z/(1 + z) = \pm 0.02$ and $\Delta z/(1 + z) = \pm 0.04$ to the EAZY-new-sm $\Pi(z)$ distributions and re-ran the computations for the $b_{\text{gal}}$ fits. This photo-$z$ bias range covers, and indeed exceeds, the overall bias expectation for EAZY (Hildebrandt et al. 2010; Dahlen et al. 2013).

The resulting redshift distributions and fitted $b_{\text{gal}}$ values are shown in Fig. 7. There is a clear trend in $b_{\text{gal}}$ due to the redshift bias.

We summarize the results of this test using the largest observed statistical error value for the overall statistical error, and the difference between the highest (lowest) observed $b_{\text{gal}}$ and the original galaxy bias as the positive (negative) systematic bias. We get $b_{\text{gal},g} = 3.90 \pm 0.30\,(\text{stat}) \pm 0.15\,(\text{sys})$ for the $g$-dropouts, $b_{\text{gal},r} = 8.44\pm0.57\,(\text{stat})\pm0.22\,(\text{sys})$ for the $r$-dropouts, and $b_{\text{gal},i} = 11.94\pm2.06\,(\text{stat})\pm0.38\,(\text{sys})$ for the $i$-dropouts.

While the above numbers do represent the systematic

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**Figure 6.** Theoretical model fits to the spherical autocorrelation power spectra of the $g$-, $r$- and $i$-dropout galaxy samples (left, center and right column, respectively). Each row corresponds to a different redshift distribution setup, indicated on the right edge. Binned empirical measurements are in solid black points and error bars, and expected Poisson shot noise is in dashed grey lines. Solid coloured lines represent non-linear theoretical model curves, fitted to the data, while dashed lines show the linear models. The resulting $b_{\text{gal}}$ linear galaxy bias fit values and statistical uncertainties are also indicated, along with the median redshift of the given redshift distribution.
effect of redshift bias, the test assumes that other details of the photo-z distribution are correct. To more thoroughly take into account potential systematics, we determine the difference between $b_{\text{gal}}$ of the fiducial $\Pi(z)$ and the largest (smallest) $b_{\text{gal}}$-value of any other redshift setup; we then add that difference to the positive (negative) systematic error. Again, the overall statistical error was chosen to be the largest observed such value for a given dropout sample.

Thus, our final, more conservative estimate for the linear galaxy bias is $b_{\text{gal},g} = 3.90 \pm 0.33(\text{stat})^{+0.64}_{-0.24}(\text{sys})$ for $g$-band dropout galaxies, with median redshift $z \approx 3.7$; $b_{\text{gal},r} = 8.44 \pm 0.63(\text{stat})^{+1.42}_{-0.72}(\text{sys})$ for $r$-band dropout galaxies at $z \approx 4.7$; and $b_{\text{gal},i} = 11.94 \pm 2.24(\text{stat})^{+1.52}_{-1.27}(\text{sys})$ for $i$-band dropout galaxies at $z \approx 5.9$.

With this choice of summarizing, we may be overestimating the systematic error by “double counting” the redshift bias, as the different $\Pi(z)$ distributions might be biased around a central value. On the other hand, we may not be taking into account all potential idiosyncrasies of redshift distributions, and thus could be underestimating the systematic error.

In the future, this question could be reasonably resolved by verifying our photo-z distribution with a statistically representative sample of spectroscopic redshifts.

6 DISCUSSION AND CONCLUSION

In this paper, we have presented a measurement of linear galaxy bias at high redshifts, using dropout galaxy catalogs in the SSP+UH survey.

The $g$-band dropout sample at $z \approx 3.7$ yields $b_{\text{gal},g} = 3.90 \pm 0.33(\text{stat})^{+0.64}_{-0.24}(\text{sys})$, the $r$-band dropout sample at $z \approx 4.7$ yields $b_{\text{gal},r} = 8.44 \pm 0.63(\text{stat})^{+1.42}_{-0.72}(\text{sys})$; and the $i$-dropout sample at $z \approx 5.9$ yields $b_{\text{gal},i} = 11.94 \pm 2.24(\text{stat})^{+1.52}_{-1.27}(\text{sys})$.

The value of the galaxy bias depends strongly on the specifics of the sample selection and, in particular, on the depth of the potential wells occupied by the galaxies we measure. Our $b_{\text{gal}}$ results are somewhat larger than expected (e.g., Tegmark & Peebles 1998), i.e. the galaxies selected by our colour cuts correspond to higher density regions on average, especially in the case of $i$-dropouts. Beyond the fact that these galaxies are situated in higher mass halos, we cannot draw further conclusions due to the uncertainties in the redshift distributions.

Our work will facilitate performing a similar analysis in the 20 square degree area of the upcoming Hawaii Two-0 survey. With an area approximately ten times larger, the statistical error in the measurement is expected to be a factor of $\sqrt{10}$ lower (e.g., Szapudi & Colombi 1996).

We have identified the largest source of our systematic error as the determination of the $\Pi(z)$ redshift distribution of the respective galaxy samples. In the future, we will obtain spectroscopic redshifts for a subset of our data with Keck DEIMOS (Faber et al. 2003). This will enable a more precise calibration of our photometric redshifts and the redshift distributions.

At present, we expressed our results in terms of the linear galaxy bias, assuming concordance ΛCDM cosmology. With the larger H20 data set and better calibrated photometric redshifts, we can constrain cosmology, in particular measure $\sigma_8$ at high redshifts. Since the galaxy power spectrum constrains $\sigma_8 \times b_{\text{gal}}$ in the linear regime, we need to add at least another measurement. The possibilities include: galaxy overdensity–weak lensing correlations; constrain the bias itself using counts-in-cells distributions (Szapudi & Pan 2004; Repp & Szapudi 2019), and then fit $\sigma_8$; compute higher-order statistics, going to three-point correlations instead of using two-point correlations only (e.g., Pan & Szapudi 2005).

In summary, we found that within the context of Planck concordance cosmology, a linear bias model adequately explains the clustering of galaxies at $z \approx 3 – 6.5$. With 10 times more data in the near future and better redshift calibration, the Hawaii Two-0 survey will produce high-redshift
constraints on cosmological parameters and galaxy formation.

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Appendix A: An Analysis of Magnification Bias

The $\delta_{\text{gal}}(\theta)$ galaxy overdensity that is observed in magnitude-limited galaxy samples can be modulated by an effect known as magnification bias. Foreground matter density can enhance (or diminish) observed source counts via weak gravitational lensing, by pushing sources above (or below) the detection limit. Here we provide an analysis of how magnification bias affects our results.

First, we give a short summary of how the modelling described in Sect. 3 changes due to the inclusion of magnification bias. The formulae are based on the works of Hui, Gaztañaga & Loverde (2007); Loverde, Hui & Gaztañaga (2008); Ziour & Hui (2008); Joachimi & Bridle (2010), refer to these for more theoretical details.

Instead of measuring the galaxy overdensity directly, the overdensity we observe can be written as

$$\delta_{\text{O}}(\theta) = \delta_{\text{gal}}(\theta) + \delta_{\mu}(\theta),$$

(A1)

where $O$ denotes observed, and $\mu$ denotes the magnification contribution.

Accordingly, the empirical spherical autocorrelation power spectrum of this observed overdensity becomes $C^{\delta \delta}_{\text{O}}$, and the theoretical model for it is

$$C^{\delta \delta}_{\text{O}} = C^{\delta \delta}_{\text{gal}} + 2C^{\mu \mu}_{\text{gal}} + C^{\mu \mu}_{\text{pp}}.$$  

(A2)

The $\delta_{\text{gal}}$ and $\delta_{\mu}$ terms can be computed through the analogues of Eq. 6,

$$C^{\delta \mu}_{\text{gal}} = \frac{2}{\pi} \int dk k^2 \langle G^l_\mu(k) \rangle \langle G^l_\mu(k) \rangle$$

(A3)

and

$$C^{\mu \mu}_{\text{pp}} = \frac{2}{\pi} \int dk k^2 \langle G^l_\mu(k) \rangle \langle G^l_\mu(k) \rangle,$$

(A4)

where we introduced the kernel function for lensing magnification

$$[G^l_\mu(k)] = (5s - 2) \frac{3H_0^2\Omega_m}{2c} \times$$

$$\times \int d\tau g(z(\tau)) (1 + z(\tau)) P_s(k, z(\tau)) j_l(\chi(\tau) k).$$

(A5)

Above, $H_0$ is the Hubble constant at present time, $\Omega_m$ denotes the cosmological mass density parameter, $c$ is the speed of light,

$$s = \frac{d \log_{10} N(< m)}{dm}|_{m_0}$$

is the slope of the galaxy number count function at the limiting magnitude $m_0$, and finally

$$g(z) = \chi(z) \int_{z}^{\infty} dz' \frac{\chi(z') - \chi(z)}{\chi(z')} \Pi(z)$$

(A7)

is the lensing weight function.

Again, we adopt the Limber approximation (Limber 1953) to speed up the computation, yielding

$$C^{\mu \mu}_{\text{pp}} = (5s - 2) \frac{3H_0^2\Omega_m}{2c} \int d\tau \frac{1}{c\chi^2(\tau)} P_s(k, z(\tau)) \times$$

$$\times b(z(\tau)) \Pi(z) \left( \frac{dz}{d\tau} \right) g(z(\tau))(1 + z(\tau))$$

(A8)

and

$$C^{\mu \mu}_{\text{pp}} = (5s - 2)^2 \left( \frac{3H_0^2\Omega_m}{2c} \right)^2 \int d\tau \frac{1}{c\chi^4(\tau)} P_s(k, z(\tau)) \times$$

$$\times g^2(z(\tau))(1 + z(\tau))^2.$$  

(A9)

Examining the components of $C^{\delta \delta}_{\text{O}}$ in Eq. A2, it is clear that $C^{\delta \delta}_{\text{gal}}$ scales with $b^2_{\text{gal}}$ (see Eq. 9), $C^{\mu \mu}_{\text{gal}}$ scales with $b_{\text{gal}}$, and $C^{\mu \mu}_{\text{pp}}$ does not depend on the galaxy bias.

We evaluated the theoretical expressions via SPHERICOSMO, and performed the linear galaxy bias fit on the dropout samples using our fiducial EAZY-new-sm $\Pi(z)$ distribution.

The results are $b_{\text{gal},g} = 3.89 \pm 0.29$, $b_{\text{gal},r} = 8.44 \pm 0.55$ and $b_{\text{gal},i} = 11.93 \pm 2.00$ (statistical error only) for the three dropout galaxy samples. These values are indistinguishable from the original EAZY-new-sm results (see Fig. 6), which did not take into account magnification bias.

The reason why the results are unaffected by magnification bias can be illustrated by comparing the components of $C^{\delta \delta}_{\text{O}}$, shown in Fig. A1. It is clear that $C^{\mu \mu}_{\text{pp}}$ and $C^{\mu \mu}_{\text{gal}}$ are orders of magnitude smaller than $C^{\delta \delta}_{\text{gal}}$ at all considered $l$ values.

We note that $C^{\mu \mu}_{\text{pp}}$ and $C^{\mu \mu}_{\text{gal}}$ scale with the factor $(5s - 2)$ and $(5s - 2)^2$. The number count slope was determined to be $s = 0.11$ for $g$-dropouts, $s = 0.13$ for $r$-dropouts, and $s = 0.16$ for $i$-dropouts, based on the $i$, $z$ and $y$ magnitude distributions, respectively. The value of $s$ depends on the exact choice of limiting magnitude at the edge of the sample, but the credible interval for all dropout samples certainly does not extend beyond the range $[0.0, 0.3]$. Within this range, $(5s - 2)$ is small enough that the magnification contribution remains inconsequential.

We conclude that, at the precision currently allowed by our data, the effect of magnification bias is negligible.
Figure A1. Additive components of the $C_{l}^{\Omega\Omega}$ theoretical spherical autocorrelation power spectra (see Eq. A2), for the $g$-, $r$- and $i$-band dropout galaxy samples, from left to right. Solid lines show $C_{l}^{gg}$, dotted lines show $C_{l}^{\mu\mu}$, and dashed lines show $|2C_{l}^{g\mu}|$. The sign of $C_{l}^{g\mu}$ is negative, at all $l$ values.