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T-wave alternans and arrhythmogenesis in cardiac diseases

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T-wave alternans, a manifestation of repolarization alternans at the cellular level, is associated with lethal cardiac arrhythmias and sudden cardiac death. At the cellular level, several mechanisms can produce repolarization alternans, including: (1) electrical restitution resulting from collective ion channel recovery, which usually occurs at fast heart rates but can also occur at normal heart rates when action potential is prolonged resulting in a short diastolic interval; (2) the transient outward current, which tends to occur at normal or slow heart rates; (3) the dynamics of early afterdepolarizations, which tends to occur during bradycardia; and (4) intracellular calcium cycling alternans through its interaction with membrane voltage. In this review, we summarize the cellular mechanisms of alternans arising from these different mechanisms, and discuss their roles in arrhythmogenesis in the setting of cardiac disease.

Keywords: T-wave alternans, arrhythmias, restitution, calcium cycling, afterdepolarizations, cardiac diseases

INTRODUCTION

T-wave alternans (TWA), a precursor of lethal cardiac arrhythmias and sudden death (Rosenbaum et al., 1994; Armoundas et al., 2002; Narayan, 2006; Verrier and Nieminen, 2010b), has been associated with many cardiac diseases, such as heart failure (Luomanmaki et al., 1975), long QT syndromes (Zareba et al., 1994; Shimizu and Antzelevitch, 1999; Armoundas et al., 2000; Kroll and Gettes, 2002; Wegener et al., 2008; Verrier and Nieminen, 2010a), ischemia (Nakashima et al., 1978; Giudici and Savage, 1990), Brugada syndrome (Chinushi et al., 2001; Morita et al., 2002, 2006; Takagi et al., 2002; Nishizaki et al., 2005; Fish and Antzelevitch, 2008; Tada et al., 2008), etc. TWA is a manifestation of cellular repolarization alternans and can also result from localized 2:1 block in tissue. Several mechanisms of repolarization alternans have been demonstrated and linked to arrhythmogenesis in different diseases. Understanding the mechanisms of TWA for different diseases is important for developing antiarrhythmic strategies. Here we review recent progress on understanding cardiac alternans to provide readers an integrative view of TWA on cardiac arrhythmogenesis. We summarize the following aspects of alternans: the dynamical mechanisms, ionic mechanisms underlying the dynamical factors, and how different mechanisms may lead to arrhythmias in different diseases.

ALTERNANS DUE TO ELECTRICAL RESTITUTION RESULTING FROM COLLECTIVE ION CHANNEL RECOVERY

Alternans may occur at very fast heart rates (200–300 bpm) (Karagueuzian et al., 1993; Koller et al., 1998; Cao et al., 1999; Pastore et al., 1999; Christini et al., 2006; Hayashi et al., 2007; Mironov et al., 2008), and is promoted by a steep slope of action potential duration (APD) restitution at short diastolic interval (DI). APD restitution, defined as the dependence of APD on the preceding DI, is determined by the collective recovery of many ionic currents. In tissue, conduction velocity (CV) also slows at short DI, known as CV restitution, which is a key dynamical factor promoting spatially discordant APD alternans.

APD AND CV RESTITUTION

Action potential duration is traditionally defined by a voltage criterion, such as 90% recovery from the peak voltage, or simply by setting a voltage threshold above and below which the time duration is defined as APD or DI, respectively. APD restitution can be measured by gradually incrementing the pacing cycle length (PCL), or suddenly altering the coupling interval between two consecutive beats to change the DI (Figure 1A). In general, a shorter DI gives rise to a shorter APD due to incomplete recovery of the ion channels, such that APD typically decreases monotonically as DI decreases (Figure 1B) (Nolasco and Dahlen, 1968; Koller et al., 1998; Goldhaber et al., 2005). However, non-monotonic APD restitution curves have also been observed (Franz et al., 1988; Watanabe et al., 1995). CV restitution curves can be similarly defined by a plot of CV versus DI (Figure 1C) (Qu et al., 1999).

The slope of the APD restitution curve is a collective measure of the recovery processes of all the ion channels and their interactions with voltage during the action potential (Qu et al., 2000b). Since Na channels recover from inactivation quickly, their effect on APD restitution occur mainly in the short DI range (0–40 ms) but can be extended to long DIs under ischemic conditions (Qu et al., 2004) in which Na channel recovery is slowed (Joyner et al., 1991; Pu and Boyd, 1997). Since normal Na channels are mainly inactivated during the plateau of the AP, they have minor direct effects on APD, but incomplete recovery of Na channel reduces the amplitude of the action potential, which affects the activation of other channels influencing APD. Since the action potential upstroke is determined by Na channel, CV restitution is almost completely governed by Na channel recovery (Qu et al., 2004).
The L-type Ca channel (LCC) recovers more slowly than the Na channel, and its effect is manifested at short and intermediate DI ranges (0–100 ms). Since LCC provide the major inward current maintaining the action potential plateau, APD is more sensitive to LCC than other channels, so that LCC recovery plays a major role on APD restitution slope. Blocking LCC reduces the slope of APD restitution curve. Time-dependent K channels (such as $I_{Ks}$ and $I_{Kr}$) recover even more slowly, so their effects span to a much longer DI range. However, due to reverse use-dependence (Hondeghem and Snyders, 1990), K channels also have non-trivial effects on the slope of APD restitution at short and intermediate DI ranges, and blocking K channels generally steepens the APD restitution curve.

Due to slow recovery of ion channels or gradual accumulation of ions (Hund and Rudy, 2000; Fox et al., 2002a,c; Li and Otani, 2003; Kalb et al., 2004; Goldhaber et al., 2005), cardiac myocytes exhibit memory. For example, the S1S2 APD restitution curves depend on the S1 PCL (Boyett and Jewell, 1978; Elharrar and Surawicz, 1983; Franz et al., 1983; Bjornstad et al., 1993; Koller et al., 1998; Kalb et al., 2004). Similarly, if the PCL changes suddenly (from long to short, or short to long), it takes many beats for APD to accommodate to the steady state (Franz et al., 1988; Watanabe and Koller, 2002). In the presence of memory, APD does not depend solely on the previous DI, but on a longer history of remote DIs and APD’s (Choi et al., 2004).

**MECHANISM OF ALTERNANS PROMOTED BY A STEEP APD RESTITUTION CURVE**

The mechanism of APD alternans was first elucidated by Nolasco and Dahlen (1968) who used graphical method to show that APD alternans occurred when the slope of the APD restitution curve was greater than one. Assume no cardiac memory, APD restitution is defined as the functional relationship between APD and its previous DI. Under this condition, one can denote the APD restitution by the following equation (see Figure 2A for notion):

$$APD_{n+1} = f(DI_n),$$

(1)

Also, PCL is the summation of the APD and DI at any beat $n$ (see Figure 2A), i.e.,

$$PCL = APD_n + DI_n.$$  

(2)

For each PCL, there is a steady state or equilibrium point. Graphically, the equilibrium point is the intersection point (Figures 2B and C) of the restitution curve (Eq. 1) and the straight line (Eq. 2). When the slope of APD restitution curve at the equilibrium point is smaller than unity, as illustrated in Figure 2B, APD and DI, which are initially away from their equilibrium values, approach their equilibrium values as more and more iterations occur, eventually converging to the equilibrium point. Therefore, the equilibrium point is stable. Note that the system develops transient alternans and the smaller the slope, the faster APD alternans disappears. However, if the heart rate is fast so that the slope of the APD restitution curve at the equilibrium point is greater than unity, then this equilibrium point is unstable (Figure 2C). In this case, any perturbation of DI or APD from its equilibrium value will grow in amplitude. For a linear APD restitution curve, the amplitude of alternans will keep on growing until 2:1 block occurs. Since in general the slope of APD restitution curve becomes smaller for larger DI, the growth rate will be attenuated by the shallow slope region of the curve, and eventually the system may settle into a new state that alternates between two states, resulting in stable APD alternans. Figure 3 shows how two APD restitution curves with different slope properties respond differently to periodic pacing. For the restitution curve with slope smaller than one everywhere (gray line in Figure 3A), the equilibrium state is always stable, i.e., a stable 1:1 response occurs for all pacing rates until 2:1 activation occurs (Figure 3B). For the restitution curve with slope greater than one at short DI, APD alternans, and other complex dynamics can occur (Figure 3C). In this case, as PCL decreases, bifurcations from the stable equilibrium state (1:1) to alternans (2:2), from 2:2 alternans to 2:1 block are observed, and more complex AP dynamics at faster pacing rates. Although the two APD restitution curves do not look very different except for their slopes, the responses to periodic pacing are dramatically different. Note that the structure of the bifurcation shown Figure 3C is very similar to that of an experimental...
bifurcation diagram (Figure 3D) (Chialvo et al., 1990), indicating that the non-linear dynamics caused by steep APD restitution may indeed be responsible for the complex dynamics observed in real cardiac myocytes.

In reality, due to memory effects, APD relies on more than just the previous DI, i.e., \( APD_{n+1} = f(DI_n, DI_{n-1}, \ldots) \). In addition, due to slow APD adaptation to PCL change, it may take many seconds for APD to reach its steady state value (Franz et al., 1988; Franz, 2003), and thus depending on the number of S1 beats given, the S1S2 APD becomes shorter (Franz et al., 1988; Franz, 2003), and APD restitution curve becomes less steep (Baher et al., 2007), and thus alternans caused by initially steep APD restitution curve may only be transient, which will eventually disappear due to APD shortening and slope reduction. Therefore, in the presence of memory, the slope of the S1S2 APD restitution (or any type of APD restitution curve (Koller et al., 1998; Kalb et al., 2004; Goldhaber et al., 2005) cannot be used to accurately predict the existence of steady state alternans, and more complicated non-linear dynamics analyses are required (Fox et al., 2002a). The slope of APD restitution curve may also fail to predict the onset of alternans when Ca cycling has a strong influence on action potential, as the Ca cycling system can itself exhibit alternans (Goldhaber et al., 2005; Shiferaw et al., 2003; Qu et al., 2007). APD restitution slope is also not an accurate parameter for predicting alternans under certain other conditions, as shown in simulations of atrial myocytes (Xie et al., 2002) and in experiments in ventricular myocytes during hypokalemia (Osadchii et al., 2010), in which effective refractory period (ERP) restitution is a better indicator. Another case is acute and chronic ischemia in which postpolarization refractoriness is present (Janse and Wit, 1989), so that APD no longer approximate ERP. In this case, the ERP restitution slope may be a better indicator for instability, which needs to be evaluated in future studies.

CV RESTITUTION AND SPATIALLY DISCORDANT ALTERNANS

In cardiac tissue, APD alternans can be either spatially concordant or spatially discordant (Cao et al., 1999; Pastore et al., 1999; Qian et al., 2001; Hayashi et al., 2007). In discordant alternans, APD is long throughout the entire tissue on one beat and short throughout the next beat (Figure 4A). In discordant alternans, which occurs at shorter PCLs, APD alternates out of phase in neighboring regions (Figure 4B), i.e., APD is long in one region and short in an adjacent region on one beat, and changes phase on the next beat. CV restitution as a mechanism of spatially discordant alternans was first shown by Cao et al. (1999), and was more rigorously proven in later theoretical studies (Qu et al., 2000a; Echebarria and Karma, 2002), and demonstrated in experiments (Hayashi et al., 2007; Mironov et al., 2008). The major conclusion is that if APD alternans occurs in a DI range in which CV is not also changing, alternans in tissue is spatially discordant. However, if APD alternans occurs in the DI range in which CV is also varying with DI (at short DI), then spatially discordant alternans can form if the tissue size is adequate. Since the QT interval and the T-wave in ECG correlate with APD and its spatial distribution, APD alternans is manifested as TWA in ECG. During spatially discordant alternans, CV varies, which affects the width and amplitude of QRS in ECG, resulting in both T-wave and QRS alternans. This prediction agrees with the experimental observation that only TWA occurred during discordant alternans (bottom panel of Figure 4A), but both QRS and TWA occurred during discordant alternans (bottom panel of Figure 4B).

ARRHYTHMOGENESIS

The arrhythmogenic effects of APD alternans due to steep APD restitution curve occurring at short DIs can be understood as follows. First, spatially discordant alternans results in large spatial and slope reduction. Therefore, in the presence of memory, the slope of the S1S2 APD restitution curve (or any type of APD restitution curve (Koller et al., 1998; Kalb et al., 2004; Goldhaber et al., 2005) cannot be used to accurately predict the existence of steady state alternans, and more complicated non-linear dynamics analyses are required (Fox et al., 2002a). The slope of APD restitution curve may also fail to predict the onset of alternans when Ca cycling has a strong influence on action potential, as the Ca cycling system can itself exhibit alternans (Goldhaber et al., 2005; Shiferaw et al., 2003; Qu et al., 2007). APD restitution slope is also not an accurate parameter for predicting alternans under certain other conditions, as shown in simulations of atrial myocytes (Xie et al., 2002) and in experiments in ventricular myocytes during hypokalemia (Osadchii et al., 2010), in which effective refractory period (ERP) restitution is a better indicator. Another case is acute and chronic ischemia in which postpolarization refractoriness is present (Janse and Wit, 1989), so that APD no longer approximate ERP. In this case, the ERP restitution slope may be a better indicator for instability, which needs to be evaluated in future studies.

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APD restitution curve, even at normal heart rates. Another example is ischemia, in which the Na channel conductance is reduced and recovery slowed (Joyner et al., 1991; Pu and Boyden, 1997), causing postrepolarization refractoriness. This not only broadens the range over which CV restitution occurs, potentiating spatially discordant alternans, but it also makes alternans occur at slower heart rates (Qu et al., 2004).

Alternans in Decreased by the Transient Outward Current ($I_o$)

In an experimental study in isolated canine ventricular tissue and myocytes, Lukas and Antzelevitch (1993) showed that APD alternans occurred in epicardial myocytes under “simulated ischemia” conditions with alternating loss-of-dome of the action potential (Figure 5A). The APD alternans resolved when the outward transient current ($I_o$) was blocked, indicating that the alternans was associated with $I_o$. In a recent modeling study, Hopenfeld (2006) was able to simulate the same alternans phenomenon and show that the alternans was caused by

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**FIGURE 3** | Action potential duration alternans and complex dynamics due to APD restitution. (A) APD restitution curves with different slope properties. Inset shows the slopes of the two APD restitution curves. (B) A bifurcation diagram by plotting APD versus PCL for the shallow APD restitution curve. The figure was obtained by iterating Eqs. 1 and 2 with many iterations for a given PCL. For each PCL, the first 100 APDs were dropped and the next 100 APDs were plotted. Since the equilibrium point is always stable, only one point for each PCL shows up on the plot in this case. However, if alternans (or chaos) occurs, two (or many) APD points will show up as is the case in C. (C) A bifurcation diagram for the steep APD restitution curve. (D) Bifurcation diagram from an experiment (Chialvo et al., 1990).
the interaction of $I_{n}$ and $I_{Ca,L}$. By adding $I_{n}$ to the Luo–Rudy
phase 1 (LR1) model (Luo and Rudy, 1991), one can also easily
induce APD alternans similar to the experimental observations
(Figure 5B). This type of APD alternans can also be induced
by fibroblast–myocyte coupling since fibroblast–myocyte cou-
ping generates a gap junction current to the myocyte similar
to $I_{n}$ (Xie et al., 2009). Different from alternans in other condi-
tions (Karagueuzian et al., 1993; Koller et al., 1998; Cao et al.,
1999; Pastore et al., 1999; Christini et al., 2006; Hayashi et al.,
2007; Mironov et al., 2008), alternans in this case occurs at
normal heart rates (PCL 800 ms or 75 bpm) where the DI is
still very long. $I_{n}$-mediated spike-and-dome action potential
morphology is linked to Brugada syndrome, and TWA is widely
observed in Brugada syndrome (Chinushi et al., 2001; Morita
et al., 2002, 2006; Takagi et al., 2002; Nishizaki et al., 2005; Fish
and Antzelevitch, 2008; Tada et al., 2008). In agreement with the
$I_{n}$-mediated APD alternans shown in Figures 5A and B, TWA in
Brugada syndrome also occurs at normal heart rates in which
the DIs (TQ intervals in the ECG) of the alternating beats are
still very long (Figure 5C) (Nishizaki et al., 2005).

**FIGURE 4** Spatially concordant and discordant alternans (modified from Pastore et al. (1999)). (A) Concordant alternans. Top: $\Delta$APD = APD$_{n}$ – APD$_{n+1}$

distribution in space; Middle: sample action potential recordings for two

consecutive beats from the sites marked on the upper panel; Bottom:
Pseudo-ECG showing TWA. Since APD alternans is concordant, the color in the
top panel is uniform in space ($\Delta$APD everywhere is positive in one beat and

negative in the following beat) and since no CV restitution is engaged, no QRS

alternans in the ECG. (B) Same as A but for discordant alternans. Since APD

alternans is discordant, the color in the top panel is no longer uniform in space,

but change from one to the other ($\Delta$APD changes from negative to positive as the

color changes from blue to red in space, and color map reverse in the following

beat), and since CV restitution is engaged, QRS alternans occurs in the ECG.
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variable $x$ at the moment of stimulation (i.e., the initial value of $x$, denoted as $x_0$) while maintaining the initial values of the other variables unchanged (Figure 6C), and plot APD versus this initial $x$ value in Figure 6D. As $x$ increases, the action potential gradually loses its spike-and-dome morphology, which results in a sensitive dependence of APD on $x$. The sensitive range occurs at the small $x$ values, which means that the $x$ gate is almost recovered, explaining why APD is sensitive to small changes in DI in slow heart rates. As to why the spike-and-dome morphology is...
sensitive to the K channel recovery, this is a complex issue. As shown by Greenstein et al. (2000), $I_{\text{aKL}}$ plays an important but complex role in regulating the action potential morphology and duration. The APD restitution property in the presence of $I_{\text{aKL}}$ is due to a complex interaction among $I_{\text{aKL}}$, $I_{\text{aK}}$ and $I_{\text{aKL}}$. We will present a detailed dynamical analysis on this issue in a future publication (unpublished data). Also note that in real systems, other slow changes, such as the slow recovery of $I_{\text{aKL}}$ itself, can be responsible to the sensitivity at slow heart rate, not necessarily the K channel recovery per se.

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Since $I_{\text{aKL}}$-mediated APD alternans occurs at normal heart rates at which the DIs of the alternating beats are still very long, CV restitution may not be engaged. Therefore, spatially discordant alternans mediated by CV restitution is not likely to occur. For the same reason, 2:1 regional conduction block due to wave front–tail interaction is also unlikely. Therefore, whether alternans induced by $I_{\text{aKL}}$ or TWA in Brugada syndrome has any causal relationship to arrhythmogenesis is unclear. On the other hand, phase-2 reentry has been proposed as a tissue mechanism of arrhythmias in Brugada syndrome (Antzelevitch, 1999; Yan and Antzelevitch, 1999; Morita et al., 2006; Fish and Antzelevitch, 2008). In phase-2 reentry, action potential with a spike-and-dome morphology in one region reenters a neighboring region with earlier recovery due a shorter APD without a dome. Computer simulations simply following this hypothesis showed that phase-2 reentry could be induced only in narrow parameter regions even when the large spike-and-dome morphology is maximized (Miyoshi et al., 2003, 2005; Maoz et al., 2009). In a recent study, Maoz et al. (2009) showed that when alternans and other complex APD patterns occurred, phase-2 reentry could be induced in a much wider parameter range, even in homogeneous tissue (Figure 7). This indicates that dynamical instabilities that cause alternans and other complex action potential dynamics are sensitive to the K channel recovery, this is a complex issue. As shown by Greenstein et al. (2000), $I_{\text{aKL}}$ plays an important but complex role in regulating the action potential morphology and duration. The APD restitution property in the presence of $I_{\text{aKL}}$ is due to a complex interaction among $I_{\text{aKL}}$, $I_{\text{aK}}$ and $I_{\text{aKL}}$. We will present a detailed dynamical analysis on this issue in a future publication (unpublished data). Also note that in real systems, other slow changes, such as the slow recovery of $I_{\text{aKL}}$ itself, can be responsible to the sensitivity at slow heart rate, not necessarily the K channel recovery per se.

**FIGURE 7** Phase-2 reentry due to dynamical instabilities (Modified from Maoz et al. (2009)). (A) Phase-2 reentry in a homogeneous 1D cable ($I_{\text{aKL}}$ distribution in C). On the first beat shown, the action potential is long and exhibits spike-and-dome morphology for all cells. On the second and third beats, the action potential is short with no dome. On the fourth beat (close-up in B), however, the action potential becomes spatially heterogeneous, cells close to the pacing site (+) exhibit spike-and-dome morphology and distal cells lose the dome, leading to an anterograde phase-2 reentry (arrow). (D) Phase-2 reentry in a heterogeneous cable ($I_{\text{aKL}}$ distribution in F). In the small $I_{\text{aKL}}$ region, the action potential morphology is always stable, but in the large $I_{\text{aKL}}$ region, the action potential morphology is unstable, forming retrograde phase-2 reentry on the third beat (Close-up in E).
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time-dependent K currents, such as $I_{Ks}$, enter more deeply closed states, and thus are less activated during an action potential (Silva and Rudy, 2005). However, EADs can also occur at fast heart rates (Huffaker et al., 2004), due to Ca accumulation enhancing inward currents, such as $I_{NCX}$ or the Ca-activated non-selective cation current $I_{ns(Ca)}$, especially in late phase 3 when inward $I_{NCX}$ is potentiated by negative membrane potential (Luo and Rudy, 1994).

**AlternAns resulting from EADs**

Despite the various complex ionic mechanisms, we showed recently that EADs are caused by dynamical instabilities and can exhibit many complex temporal patterns including APD alternans under periodic pacing (Sato et al., 2009, 2010; Tran et al., 2009). The major non-linear dynamics can also be captured by the APD restitution curve. When EADs are present, the APD restitution curve becomes non-monotonic and discontinuous (black lines in Figure 8B). As DI increases, APD first increases steeply, after which a discontinuous jump occurs [where one more EAD occurs in the action potential (Figure 8A)] and then APD decreases and saturates. Using the same cobweb technique as shown in Figure 2, one can obtain complex action potential dynamics including alternans (Figure 8C). The cobweb in Figure 8B illustrates how APD alternans forms in this system. Figure 8D shows a simulation in a 1D cable, demonstrating that EAD alternans causes TWA. The ECG morphology from the simulation agrees well with TWA recorded from a long QT patient (Figure 8E) (Wegener et al., 2008).

**Ionic mechanisms of EADs**

Early afterdepolarizations (EADs) are abnormal depolarizations occurring during the plateau or the repolarizing phase of the action potential (Figure 8A). EADs usually occur in the setting of reduced repolarization reserve (Roden, 1998), which can result from a reduction in outward currents, or an increase in inward currents, or both. Specifically, EADs can be induced by reducing the outward currents, such as the two components of the time-dependent potassium current ($I_{Ks}$ and $I_{Kr}$) (Keating and Sanguinetti, 2001; Sanguinetti and Tristani-Firouzi, 2006), which are the causes of arrhythmias for LQT1 and LQT2. EADs can also be induced by promoting the late sodium current ($I_{Na}$) (Clancy and Rudy, 1999; Song et al., 2006), which is the cause of arrhythmias for LQT3; by increasing the window $I_{Ca,L}$ (January and Riddle, 1989; Antoons et al., 2007); or by increasing $I_{NCX}$ (Luo and Rudy, 1994; Burashnikov and Antzelevitch, 1998). EADs can also occur when the myocyte is overloaded with Ca causing spontaneous SR Ca release in systole (Volders et al., 2000). Classically, EADs emerge during bradycardia, since repolarization reserve is reduced because of the slow diastolic depolarization. However, at fast heart rates, EADs can also occur due to Ca accumulation enhancing inward currents, such as $I_{NCX}$ or the Ca-activated non-selective cation current $I_{ns(Ca)}$, especially in late phase 3 when inward $I_{NCX}$ is potentiated by negative membrane potential (Luo and Rudy, 1994).

**AlternAns resulting from early afterdepolarization dynamics**

Figure 8 | Action potential duration alternans resulting from EAD dynamics. (A) S1S2 restitution protocol (as explained in Figure 1A). After the S1 beat, two S2 beats are shown in which the DI of the read trace is 1 ms larger than the blue one, showing that at the APD discontinuous point, a very small increase in DI results in an action potential with an EAD. (B) S1S2 APD restitution curve (black lines) when EADs occur at slow heart rates. The discontinuous jump in APD indicates that the action potential changes from no EAD to one EAD, or from one to two EADs, an all-or-none behavior. The cyan line satisfying $PCL = APD_n + DI_n$. The arrowed blue lines illustrated cobweb diagram leading to alternans (red dashed square). (C) A bifurcation diagram showing steady state APD versus PCL obtained by iterating the map as shown in B. The numbers indicate number of EADs in an action potential for the corresponding APD value. (D) Simulation results of a 1D cable showing EAD alternans and TWA. (E) ECG showing TWA from a patient with drug-induced long QT syndrome (Wegener et al., 2008). Panels A–C were modified from Sato et al., 2009, 2010.
ARRHYTHMOGENESIS
While EADs are known to increase substrates vulnerability (by increasing APD dispersion) and promote triggers (PVCs) for reentry formation, especially in long QT syndromes and heart failure, the role of EAD-induced TWA in arrhythmogenesis is not known. On the other hand, TWA is frequently observed in long QT patients and often precedes Torsades de Pointes (Tdp) (Armondas et al., 2000; Kroll and Gettes, 2002; Wegener et al., 2008; Verrier and Nieminen, 2010a). TWA in long QT syndromes can be caused by steep APD restitution at short DI, especially since APD is prolonged which shortens DI at all heart rates. However, as shown in Figure 8E, during TWA alternans in long QT patients, the DI (or TQ interval in the ECG) may not be short, which agrees with the mechanism of EAD-induced APD alternans at slow heart rates. In addition, multiple ectopic foci resulting from EADs have been hypothesized (Dessertenne, 1966) and demonstrated (Asano et al., 1997; Choi et al., 2002) as a mechanism of Tdp. Since EADs are associated with both TWA and Tdp, this may explain the clinical observation that TWA often precedes Tdp. The question of whether TWA plays any role in causing Tdp is not clear. However, based on our recent study (Sato et al., 2009), the dynamical instabilities caused by EADs are important for initiating arrhythmias and maintaining the multiple foci to manifest Tdp. Therefore, TWA in long QT syndromes may potentiate the substrates for Tdp, similar to the role of TWA in Brugada syndrome. Nevertheless, if both TWA and Tdp are caused by EADs, then preventing EADs can prevent the arrhythmias.

ALTERNANS ARISING FROM INSTABILITIES OF INTRACELLULAR Ca CYCLING

INTRACELLULAR Ca ALTERNANS
Action potential duration is influenced by the intracellular Ca transient, and conversely, the Ca transient affects APD. If APD alternates due to electrical instabilities, the Ca transient will also alternate. However, Ca alternans can also be primary, since it can occur under voltage clamp conditions (Chudin et al., 1999; Diaz et al., 2002, 2004; Figure 9). Thus, if voltage is not clamped, primary Ca alternans can cause APD alternans and thus TWA. Several mechanisms of Ca alternans have been described. The first mechanism, proposed by Eisner et al. (2000), postulates that Ca alternans is due to a steep non-linear dependence of sarcoplasmic reticulum (SR) Ca release upon the diastolic SR Ca load immediately preceding the release (a steep fractional release–load relationship). This mechanism requires that diastolic SR Ca load alternate concomitantly with SR Ca release. Subsequent experimental (Diaz et al., 2002, 2004; Xie et al., 2008) and theoretical (Shiferaw et al., 2003; Weiss et al., 2006; Qu et al., 2007; Tao et al., 2008) studies have provided evidence supporting this mechanism. However, later experimental studies in rabbit ventricular myocytes by Picht et al. (2006) and in cat atrial myocytes by Hüsler et al. (2000) showed that under some conditions, SR always refilled to the same level before each beat during Ca alternans, indicating that Ca alternans may not rely on SR content.

3R THEORY
In a recent study (Rovetti et al., 2010), we developed a computational model of Ca cycling which is composed of a network of coupled Ca release units (CRUs, also called couplons). In this model, Ca alternans occurs in the SR Ca load range in which the fractional release curve is steep. However, Ca alternans continues even if the SR Ca content is held constant. During Ca alternans, individual Ca sparks occur irregularly, and thus the spatial distribution of myoplasmic Ca exhibits a random spatial pattern, which changes from beat to beat (Figure 10A). Space-time plots (line-scan) exhibit random and patch-like patterns, resembling the experimental data by Diaz et al. (2002) (Figures 10B and C). Using the same “ramp pacing” protocol by Picht et al. (2006), we obtained similar SR depletion dependence on SR Ca content (Figures 10D and E). Therefore, the simulation results seem to agree with both sets of experimental observations.

FIGURE 9 | Ca alternans in a rabbit myocyte (modified from Chudin et al. (1999)). (A) APD and Ca alternans at PCL = 180 ms. (B) Same as A but the action potential was clamped, i.e., the myocyte was paced with a fixed action potential.
To develop a unified theory of Ca alternans and reconcile the contradictory experimental observations, we proposed a novel theory in which Ca alternans emerges as a collective behavior of Ca sparks, determined by three critical properties of the CRU network from which Ca sparks arise: randomness (of Ca spark activation), refractoriness (of a CRU after a Ca spark), and recruitment (Ca sparks inducing Ca sparks in adjacent CRUs). We called this theory as “3R” theory (Cui et al., 2009; Rovetti et al., 2010). Here we summarize this basic theory. As illustrated in Figure 11A, a Ca spark may occur spontaneously (due to high SR Ca load or leakiness) or be activated directly by opening of LCCs in the CRU. Due to stochastic openings of LCCs and RyRs, spontaneous or triggered sparks occur randomly. We call these types of sparks primary sparks, and assume their probability to be $\alpha$. As a consequence of Ca-induced Ca release, a spark from one CRU may recruit another neighboring CRU to spark, which has also been observed in experiments (Parker et al., 1996; Izu et al., 2007) and is the basis of Ca waves. We called this type of spark a secondary spark, and assume the recruitment probability to be $\gamma$. After a CRU sparks, it remains refractory for a certain period of time after which it becomes available for release again (Sobie et al., 2006). Taking into account these three important features, we derived a simple mathematical model for the theory which links the number of sparks at the present beat ($n+1$) to the number of Ca sparks in the previous beat ($n$) as follows (Cui et al., 2009; Rovetti et al., 2010):

$$N_{k+1} = (N_0 - \beta N_k) \left[ \alpha + (1-\alpha)f \right]$$

(3)

where $f$ is a function satisfying

$$f(\alpha, \beta, \gamma, N_k) = 1 - [1 - \alpha \gamma (1 - \beta N_k/N_0)]^n$$

(4)

where $\beta$ is the probability of recovery from a previous spark, $N_0$ is the total number of CRUs, and $n$ is number of neighbors for a CRU. Following the same procedure as for the APD restitution case, one can determine the steady state (or equilibrium) of the system and its stability. The steady state can be unstable, leading to alternans for properly chosen values of parameters $\alpha$, $\beta$, and $\gamma$. The behaviors of Eq. 3 are shown in the $\alpha$-$\gamma$ parameter space in Figure 11B, and two examples shown in Figures 11C and D. Alternans occurs in an intermediate range of $\alpha$, large $\gamma$ (high recruitment), and large $\beta$ (long refractoriness).
The parameters $\alpha$, $\beta$, and $\gamma$ are dynamical parameters which are determined by many physiological factors. For example, $\alpha$ is determined by the properties of LCCs and RyRs, such as their conductance and open probability which are also affected by the Ca content in the cytosol and SR. $\beta$ is determined by the CRU refractory properties and the cycle length of activation. The refractoriness of a CRU can be attributed to either intrinsic RyR channel properties or RyR regulation by SR luminal Ca, such as by calsequestrin binding to the RyR protein complex (Schmidt et al., 2000; Terentyev et al., 2002; Gyorke et al., 2004; Jiang et al., 2004). $\gamma$ is determined by the sensitivity of RyR opening on cytosolic Ca, Ca uptake and buffering, the Ca diffusion rate, and the spacing between CRUs, etc.

**APPLICATIONS OF THE 3R THEORY TO Ca ALTERNANS**

In the experiments by Diaz and colleagues (Diaz et al., 2002, 2004; Li et al., 2009), Ca alternans was induced by either reducing LCC open probability (with LCC blockers or mild depolarized voltage clamp pulses), or reducing RyR open probability (with RyR blockers or acidosis), this agrees with the 3R theory prediction that alternans occurs in the intermediate $\alpha$. Schmidt et al. (2000) showed in mouse heart that overexpression of calsequestrin promoted pulsus alternans and Restrepo et al. (2008) showed in a modeling study that increasing calsequestrin concentration prolonged RyR refractoriness promoted alternans, which agree with the prediction of the 3R theory that alternans occurs when $\beta$ is very large. In a recent experimental study by Cutler et al. (2009), Ca alternans was suppressed by overexpressing SERCA2a. This can also be explained by the 3R theory, since increasing SR Ca uptake causes less Ca to diffuse to the neighboring CRUs and thus makes recruitment less efficient, suppressing Ca alternans.

Many studies have shown that ischemia and heart failure promote alternans (Luomanmaki et al., 1975; Qian et al., 2001; Kapur et al., 2009; Wilson et al., 2009). Insight into the mechanisms of alternans under these diseased conditions can be also gained using the 3R theory. It has been shown that in both failing and infarct hearts (Litwin et al., 2000; Gomez et al., 2001; Harris et al., 2005), Ca release becomes asynchronous, which may be caused by a lower primary spark rate ($\alpha$) resulting from remodeling processes, such as T-tubule disruption (Brette and Orchard, 2003; Louch et al., 2006), and altered excitation–contraction coupling, etc. As indicated by the 3R theory, lower $\alpha$ and asynchronous Ca release promote Ca alternans, predisposing heart failure and ischemia to Ca alternans. In addition, the RyR cluster spacing is decreased in heart failure (Chen-Izu et al., 2007), which increases the recruitment rate. Based on the 3R theory, enhancing recruitment promotes Ca alternans.

In genetic mouse models of catecholaminergic polymorphic ventricular tachycardia (Lehnart et al., 2006; Cerrone et al., 2007), the mutated RyR becomes leaky, which is considered to be the cause of Ca waves causing delayed after depolarizations (DADs). Ca alternans has also been shown in the calstabin-2-deficient mice (Lehnart et al., 2006). When RyR becomes leaky, it becomes easier for a spark to recruit the neighboring CRU to spark, which, based on the 3R theory, can promote Ca alternans.

**ARRHYTHMOGENESIS**

Ca alternans may be responsible for TWA in many diseases such as ischemia and heart failure. Since the effects of Ca transient on arrhythmias are mediated through voltage, the coupling between voltage and Ca becomes important for arrhythmogenesis due to Ca alternans. If the coupling is weak, large amplitude Ca alternans...
results in only small amplitude APD alternans, and thus the arrhythmogenic effects of Ca alternans may be very limited. If the coupling is strong, however, such that large amplitude Ca alternans results in large amplitude APD alternans and thus larger dispersion of refractoriness, the arrhythmogenic consequences are potentiated. In addition, as shown theoretically (Shiferaw et al., 2005; Jordan and Christini, 2006, 2007; Qu et al., 2007), the interactions of APD restitution steepness and Ca cycling instabilities can synergistically cause new instabilities, leading to alternans and complex dynamics, which may substantially potentiate the effects of Ca cycling on arrhythmogenesis. Another possible mechanism linking Ca alternans to arrhythmias follows from the observation that alternans tends to occur under Ca overload condition, or when SR is leaky, which are the same conditions when Ca waves occur. In fact, our theory of spark-induced sparks and the experimental observations that Ca waves occur during alternans (Diaz et al., 2002, 2004; Blatter et al., 2003) demonstrate that Ca alternans and Ca waves are linked to each other. Therefore, the association of TWA with arrhythmias under these conditions may not be causal, but reflect a predisposition to Ca waves which induce DADs. This hypothesis needs to be evaluated theoretically and experimentally in future studies.

SUMMARY AND CONCLUSIONS

Numerous clinical and basic studies investigating TWA have greatly advanced our understanding of this dynamical phenomenon and its relation to lethal arrhythmias. In this review, we summarized different dynamical mechanisms of alternans and their possible arrhythmogenic consequences in different diseases. Figure 12 presents a schematic diagram summarizing our current understanding, ranging from ionic channel function to arrhythmia pathways in tissue. Alternans can either originate from dynamical instabilities of membrane voltage or Ca cycling or their interactions. In the voltage system, instabilities are mainly governed by electrical (APD and CV) restitution, which are determined by ion channel properties dually affected by voltage and Ca. Depending on its origin, alternans can cause arrhythmias through the following pathways: (1) spatially discordant alternans which causes large dispersion of refractoriness and thus a substrate for reentry initiation by a PVC; (2) 2:1 conduction block; (3) phase-2 reentry; (4) EAD related foci and reentry. Since EADs are rate dependent, electrical restitution also plays an important role in EAD genesis itself. In the Ca cycling system, the dynamical factors that cause Ca cycling instabilities are beginning to be understood. We recently identified the 3 R’s as dynamical factors promoting instabilities leading to Ca alternans (Cui et al., 2009; Rovetti et al., 2010). The 3 R’s are themselves collective behaviors of many sub-cellular factors, such as ion channel properties and coupling of the CRUs, etc. The key of the 3 R’s is Ca spark recruitment, or spark-induced sparks, which is required for Ca waves. Therefore, Ca alternans may be linked to arrhythmias through Ca waves causing DADs. Ca is also known to play an important role in EAD genesis (Volders et al., 2000). Although TWA is closely associated with arrhythmias and sudden death, it may not be always causal, but rather a precursor. In either case, however, alternans is definitely a manifestation of electrical instability in the heart, and understanding the mechanisms of these instabilities is essential for developing effective therapeutic strategies.

Finally, we note that besides repolarization alternans arising from dynamical instabilities described in this review, TWA can also result from regional 2:1 block. This can happen when APD in one region is substantially lengthened, such as in the long QT syndromes and heart failure, or when the refractory period is substantially lengthened due to slowed Na channel recovery (Joyner et al., 1991; Pu and Boyden, 1997; Qu et al., 2004), such as postrepolarization refractoriness in ischemia (Janse and Wit, 1989). Under these conditions, the propagation of the electrical

![Figure 12](http://example.com/figure12.png)
wave blocks locally on one beat, but then propagates successfully through the same region on the next beat, resulting in TWA as well as QRS alternans. Since conduction block is already present, reentrant arrhythmias may be easily initiated when this type of TWA occurs.

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