Atomic spin sensitive dissipation on magnetic surfaces

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We identify the mechanism of energy dissipation relevant to spin-sensitive nanomechanics including the recently introduced magnetic exchange force microscopy, where oscillating magnetic tips approach surface atomic spins. The tip-surface exchange couples spin and atom coordinates, leading to a spin-phonon problem with Caldeira-Leggett type dissipation. In the overdamped regime, that can lead to a hysteretic flip of the local spin with a large spin-dependent dissipation, even down to the very low experimental tip oscillation frequencies, describing recent observations for Fe tips on NiO. A phase transition to an underdamped regime with dramatic drop of magnetic tip dissipation should in principle be possible by tuning tip-surface distance.

In a recent intriguing magnetic exchange force microscopy experiment [1], an exquisite magnetic atomic force sensitivity was demonstrated for an atomically sharp Fe magnetic tip over the (001) surface of antiferromagnetic NiO [2]. Besides showing a different force for the two oppositely polarized surface Ni atoms — well explained by the Fe-Ni exchange available from electronic structure calculations [3] — the results also show a surprisingly different mechanical dissipation, with a gigantic excess of order 15-20 meV per cycle in the antiparallel Fe-Ni spin configuration, as compared to the parallel one.

There is no existing theory of spin-dependent tip dissipation that one could use to understand not just this result but magnetically and site sensitive dissipation phenomena in general. Here we propose to use the magnetic exchange force microscopy study as a starting point. We search for a mechanism that i) can yield a magnetic dissipation of very large magnitude, similar to exchange energies, per cycle; ii) is sensitive to the spin direction, and stronger for (nearly) antiparallel spin than a parallel one; iii) works down to the lowest frequencies. Particularly puzzling is in fact the contrast between a large and stronger for (nearly) antiparallel spin than a parallel one.

For example, a tip-induced magnetic domain with oscillating boundaries could be invoked to account for a low-frequency magnetic dissipation, but the formation of such local domains is energetically unlikely, given the localized nature of the tip perturbation: Excluding a role of tip stray fields, simple model estimates suggest that the spin deformation near a perturbed surface spin should decay just a few atomic spacings away from the tip edge. We are left with acoustic phonons, certainly never gapped, both in bulk and at the surface. Here we know however that acoustic dissipation of a localized surface oscillation vanishes in linear response theory as a high power of frequency — the lattice can follow essentially adiabatically and harmonically a sufficiently slow and weak external perturbation. A large magnetic dissipation mechanism via phonons should therefore involve phenomena far from linear response. In this Letter we describe the mechanism which we believe is at work here, and show that the nonlinear response is related to the attainment of a strong coupling overdamped spin-phonon state very well known in other contexts, giving rise to a single-spin hysteresis. That also suggests that by tuning down the perturbation intensity, a phase transition could be crossed from the overdamped to the underdamped regime, with a loss of hysteresis and a dramatic drop of dissipation. Hopefully, the present approach may serve as a prototype for nanoscale magnetic dissipation.

Consider an oscillating Fe tip over a surface Ni spin $\vec{S}_i$. All neighboring spins remain essentially unperturbed, “protected” as they are by the spin gap $\Delta$. The potential felt by an $\uparrow$ Ni atom at a distance $z$ below the Fe tip differs from that felt by a $\downarrow$ Ni [3], and one can define a spin exchange potential $V^{\text{ex}}(z) = V^{\uparrow\downarrow}(z) - V^{\downarrow\uparrow}(z)$ (assuming the Fe tip to be $\downarrow$ polarized). $V^{\text{ex}}$ can be estimated to yield an exchange force $f^{\text{ex}} = -\partial V^{\text{ex}}/\partial z$ of $\sim 0.3$ nN when the tip edge is closer than 3 Å to the surface Ni [3]. This force produces a small displacement $u_z(i)$ of the Ni atom from its equilibrium position and will result in a potential of the form $-f^{\text{ex}} S^z_i u_z(i)$ (neglecting an unimportant spin-independent term). In terms of phonon creation ($a_k^\dagger$)
and annihilation \((a_\mathbf{k})\) operators \((\mathbf{k}s\) being wave vector and polarization of the phonon mode), we thus obtain a coupling of the Ni-spin to the Na acoustic phonons of the form \(H_{\text{spinphonons}} = \sum_{\mathbf{k}s} \lambda^{(i)}_{\mathbf{k}s} (a^\dagger_{\mathbf{k}s} \sigma + a_{-\mathbf{k}s})\), where \(\lambda^{(i)}_{\mathbf{k}s} = -f^{\text{ex}} e^{-i\mathbf{k} \cdot \mathbf{r}_i} \frac{\hbar}{8 \pi M k^2 \omega_{\text{ex}}} \varepsilon_z(\mathbf{k}s); \varepsilon_z(\mathbf{k}s)\) being the eigenvector of the \(\mathbf{k}s\) phonon mode. The equilibrium physics of the spin is dictated by the small frequency behavior of the crucially important spectral density \(J(\omega) = \sum_{\mathbf{k}s} \delta(\omega - \omega_{\mathbf{k}s}) |\lambda^{(i)}_{\mathbf{k}s}|^2 = (f^{\text{ex}})^2 \frac{\hbar}{8 \pi M k^2} \sum_{\mathbf{k}s} \delta(\omega - \omega_{\mathbf{k}s}) (\varepsilon_z(\mathbf{k}s))^2 / \omega_{\mathbf{k}s}\). From the standard Debye form for the low-energy acoustic phonons in three-dimensions, we find that the small-\(\omega\) limit of \(J(\omega)\) is precisely Ohmic \(J(\omega) = \hbar^2 \alpha \omega + \cdots\) with \(\alpha = (f^{\text{ex}})^2 \frac{3\hbar^2}{8 \pi M k^2 J_{\text{tip}}}\), where \(T_D\) is the Debye temperature. An estimate, with \(f^{\text{ex}} \sim 0.3\) nN, gives a value of \(\alpha\) close to 1, which can be easily made \(> 1\) by a slightly larger \(f^{\text{ex}}\) or by a better account of the (softer) surface phonon modes. The natural Ohmic behavior of this problem is a first important result, since that is by far the most interesting case, studied for decades \([10, 11]\), and it has been previously shown to arise in tip-surface interactions \([12]\). Note that the Ohmic coupling \(\alpha\) depends on the square of the exchange force \(f^{\text{ex}}\) and is therefore dependent on the tip-atom distance \(z\). We are thus led to the physics of a single spin — the surface Ni over which the tip is oscillating — in its prototypical form, that of a driven Caldeira-Leggett (or spin-boson) Ohmic model. The model is known to possess two regimes, one underdamped and one overdamped, separated by a phase transition. In the underdamped regime the spin motion is relatively unaffected by the bath, and dissipation is small. In the overdamped regime — attained at \(\alpha > 1\) \([11]\) — the spin is effectively “trapped” by the bath as schematically portrayed in Fig. 1.

The tip-induced spin-flip processes involve in the overdamped case a new time scale \(\gamma^{-1}\) that can be much longer than the external driving period \(2\pi \omega_{\text{tip}}^{-1}\). Once \(\gamma \ll \omega_{\text{tip}},\) magnetic dissipation will arise from a sort of single-spin hysteresis, similar to effects known in bistable models \([13]\). The overdamped model predicts three crucial results regarding spin-dependent dissipation. First, dissipation is quantitatively large, because the order of magnitude of the hysteresis loop area is generally set by the tip-surface magnetic exchange, itself a large energy scale \(\sim 50\) meV \([3]\). Second, dissipation will be strong when the magnetic tip is over a surface atom with antiparallel spin (left-hand side of Fig. 1), because no tip-induced spin-flip is provoked in the latter. Third, hysteretic dissipation should depend relatively weakly on \(\omega_{\text{tip}}\), and disappear only when the tip frequency is lowered below some very low frequency \(\sim \gamma,\) itself temperature-dependent.

To describe the action of the tip on a given spin, we consider the driven spin-boson model \((h = 1):\)

\[
\mathcal{H} = \frac{\varepsilon_0}{2} \sigma_z - \left[ \frac{\varepsilon(t)}{2} \sigma_z + \frac{\Delta(t)}{2} \sigma_x \right] - \hat{X} \sigma_z + \sum_{\nu} \omega_{\nu} (b^\dagger_{\nu} b_{\nu} + \frac{1}{2}),
\]

where \(\sigma_z\) and \(\sigma_x\) are the Pauli matrices, \(b^\dagger_{\nu}\) and \(b_{\nu}\) are creation and annihilation operators for the mode \(\nu\) of the phononic bath of frequency \(\omega_{\nu}\), \(\hat{X} = \sum_{\nu} \lambda_{\nu} (b_{\nu} + b^\dagger_{\nu})\) is the bath operator to which \(\sigma_z\) is coupled, \(\lambda_{\nu}\) being the previously introduced couplings, such that \(J(\omega) = \sum_{\nu} \delta(\omega - \omega_{\nu}) |\lambda_{\nu}|^2 = \alpha \omega + \cdots\). (The slight time dependence of \(\alpha\) during the tip oscillation is neglected.) In the NiO surface, \(\varepsilon_0\) represents nearest-neighbor exchange (positive and large) plus all sources of magnetic anisotropy (including dipolar contributions), and \(z\) is the unperturbed direction of the surface atom spin due to dipolar anisotropy (a \((211)\) direction). The external magnetic tip acts in the \(xz\) plane \([2]\) at an angle \(\theta\) off the \(z\) axis,

\[
\varepsilon(t) = h \cos \theta \sin^2(\omega_{\text{tip}} t), \quad \Delta(t) = h \sin \theta \sin^2(\omega_{\text{tip}} t).
\]

We will use \(\theta\) and \(\theta + \pi\) to describe Ni spins of opposite direction. The last term describes the free phonons. To avoid problems with divergences, we have as usual a high-frequency cutoff \(\omega_c\) for the spectral density, \(J(\omega) = \alpha \omega e^{-\omega/\omega_c}\), with \(\omega_c \gg h, k_B T\). The details of the solution of this model, summarized below for the reader’s convenience, are standard. The time evolution of the system is described by a standard real-time path-integral approach \([10]\), taking care of the bath degrees of freedom through the influence-functional method \([14]\) and applying the so-called noninteracting-blip approximation, valid in the \(\alpha > 1\) overdamped case for the observables of our interest \([11, 13]\). Actually, the same overdamped behavior could be achieved in the \(\alpha < 1\) regime, but only for certain values of perturbation and temperature. In terms of the free correlation function of the \(X\) operator \(g(\tau) = \sum_{\alpha} \langle \sigma_z(\tau) \rangle,\) with \(\mathcal{S}(\tau) = \int_0^\infty d\omega \frac{J(\omega)}{\omega} (1 - \cos \omega \tau) \coth \left( \frac{\beta \omega}{2} \right)\) and \(R(\tau) = \int_0^\infty d\omega \frac{J(\omega)}{\omega} \sin \omega \tau\) (where

![Figure 1: Effective potential felt by the spin under the effect of the bosonic bath for tip over spin-up and spin-down configuration.](image-url)
β = 1/k_BT, we can compute the quantities \( F_0(t) = \Delta^2(t) \int_t^\infty d\tau \ e^{-S(\tau)} \sin [R(\tau)] \sin [\varepsilon(t)\tau] \) and \( G_0(t) = \Delta^2(t) \int_t^\infty d\tau \ e^{-S(\tau)} \cos [R(\tau)] \cos [\varepsilon(t)\tau] \). From these, as shown in [10], in the overdamped regime \( \alpha > 1 \) and with a low-frequency driving, the \( z \) component of the spin obeys a simple rate equation

\[
\frac{d}{dt} \langle \sigma_z(t) \rangle = -G_0(t) \langle \sigma_z(t) \rangle + F_0(t),
\]

that can be easily integrated. Applying the same procedure to \( \langle \sigma_x(t) \rangle \), we get similarly

\[
\frac{d}{dt} \langle \sigma_x(t) \rangle = -G_0(t) \langle \sigma_x(t) \rangle + \frac{F_0(t)\tilde{G}_0(t)}{\Delta(t)},
\]

where \( \tilde{G}_0(t) \) is defined as \( G_0(t) \), but with \( \sin[\varepsilon(t)\tau] \) in place of \( \cos[\varepsilon(t)\tau] \).

To uncover the new time scale, consider, e.g., the abrupt switching on of a perturbation at \( t = 0 \), with a constant value \( \varepsilon(t) = \bar{\varepsilon} - \varepsilon_0 \) and \( \Delta(t) = \Delta \) thereafter. In this case Eq. (3) describes an exponential relaxation towards the equilibrium value \( \langle \sigma_z(\infty) \rangle = -F_0/G_0 = -\tanh(\frac{1}{2}\beta\varepsilon) \) [11] with a decay rate \( \gamma \) given, for low temperatures, in terms of the \( \Gamma \) function: \( \gamma = (\pi/\Delta^2 \varepsilon^{2\alpha-1}/2\Gamma(2\alpha)\omega_c^{2\alpha}) \left[ 1 + \pi \alpha(2\alpha-1)(2\alpha-2)/(3\varepsilon^2) \right] \). In the overdamped regime the relevant time scale \( \gamma^{-1} \) can take large values, mainly due to the large cutoff frequency \( \omega_c \) being raised to a large exponent. Even under a comparably slow external perturbation the system can be out of its instantaneous equilibrium; and that is the origin of the hysteretic behavior.

Consider now the two-level system of Eq. (1) under the external perturbation in \( \varepsilon \). Figure 2 shows the time evolution of \( \langle \sigma_z \rangle \) and \( \langle \sigma_x \rangle \) for a system in the initial state \( \langle \sigma_z \rangle = -1 \), as obtained by numerical integration of Eqs. (3) and (4) using an adaptive Runge-Kutta algorithm [17]. The system can clearly respond to the perturbation in its own time scale, yielding two different states when the perturbation is increasing and decreasing, a clear hysteretic behavior. The values of \( \langle \sigma_x(t) \rangle \) are orders of magnitude smaller than those of \( \langle \sigma_z(t) \rangle \) due to the large \( \omega_c \). [This result is related to the universal behavior of \( \langle \sigma_z(t) \rangle \) with respect to \( \omega_c \) as opposed to the nonuniversality of \( \langle \sigma_x(t) \rangle \) [18].] The dissipated energy per cycle is

\[
W = \int_0^{2\pi/\omega} dt \left[ \langle \sigma_z(t) \rangle \frac{d\varepsilon(t)}{dt} + \langle \sigma_x(t) \rangle \frac{d\Delta(t)}{dt} \right],
\]

which is the area of the hysteresis cycle in a (state-perturbation) \( \langle \sigma_z(t) \rangle - \varepsilon(t) \) diagram. Figure 3 shows the hysteresis cycle for the \( z \) component of perturbations with different angles \( \theta \), together with the angular dependence of the hysteresis area (inset). When the tip and atom spins are (even roughly) opposite, the action of exchange to overturn the spin leads to a hysteresis loop and a large dissipation: when they are nearly parallel, the loop collapses and correspondingly the magnetic tip dissipation drops. (Data for the \( x \) component, not shown, are negligible.)

We may finally address the frequency and temperature dependence of the total magnetic dissipation. Loop areas (in steady state) for different temperatures as a function of frequency are shown in Fig. 4(a). There clearly is an optimal frequency attaining maximal area. At excessive tip frequencies the spin remains effectively frozen in its trapped state; at very low frequencies the spin has plenty of time to relax and follow adiabatically the equilibrium value demanded by the tip: in both cases the loop area collapses. The inset of Fig. 4(a) shows how the optimal frequency increases with increasing temperature, reflecting the \( T \) dependence of \( \gamma \) shown in the forcing-free case. These results are consistent with what is known in the context of quantum stochastic resonance [19]. Figure 4(b) contains the same data in the form of \( P = \omega W \), the

\[ W \]

\[ x^2 \]

\[ y^2 \]

\[ z^2 \]

\[ \text{Figure 2: (Color online) Time evolution of } \langle \sigma_z \rangle \text{ (black full line, left-hand axis) and } \langle \sigma_x \rangle \text{ (dashed red line, right-hand axis) for } \varepsilon_0 = 1, \omega_c = 20\varepsilon_0, \alpha = 2.1, h = 1.5\varepsilon_0, \theta = 0.6, \omega_{tip} = 10^{-9}\varepsilon_0, \beta\varepsilon_0 = 20. \text{ The dotted line shows the shape of the external perturbation.} \]

\[ x^2 \]

\[ y^2 \]

\[ z^2 \]

\[ \text{Figure 3: (Color online) Hysteresis cycle for the } z \text{ component of the external perturbation for different angles } \theta \text{ (see legend) for } \varepsilon_0 = 1, \omega_c = 100\varepsilon_0, \alpha = 2.1, h = 13\varepsilon_0, \omega_{tip} = 10^{-12}\varepsilon_0. \text{ Inset: Angular dependence of the hysteresis area } W. \]
dramatically reducing the hysteretic behavior, as expected the faster evolution timescale to sup-
the function of frequency for various values of $\alpha$ (see legend).

In conclusion, our main novelties are that in surface magnetic tip dissipation problems, energy dissipation should be mostly mechanical and non-spin-wave, since spin waves are generally gapped by anisotropy; that spin-dependent coupling to surface atomic motion and to phonons can lead to a sort of single-site magnetic hysteresis; and finally that due to hysteresis the magnetic tip dissipation per cycle can be as large as intrasurface exchange coupling, as is seen experimentally. Further experimental possibilities will be to test the frequency, temperature and $\theta$ angle dependencies. Last but not least, the modification of the coupling parameter with the tip-sample interaction force should in principle cause a phase transition from an overdamped to an underdamped regime, with a strong suppression of dissipation at large distances and weaker couplings. We believe that these concepts should be of more general impact beyond the simple case treated here.

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Figure 4: (Color online) (a) Area of the hysteresis loop as a function of frequency for various values of $\beta$ (see legend). Inset: Frequency of maximum area of the hysteresis loop as a function of the temperature $T$. (b) Dissipated energy as a function of frequency for various values of $\beta$ (see legend).

dissipated power. At low frequencies $P$ increases as a power law (roughly $\omega^2$), eventually reaching a plateau where the dissipation levels off over a wide frequency range. Other mechanisms will of course play a role at higher frequencies, but hysteretic dissipation is the only relevant nonlinear one that survives down to experimentally relevant low frequencies.

The magnetic dissipation per cycle produced by the mechanism identified satisfies all desired requisites, since it is (i) large, and of the same order of magnitude of the antiferromagnetic exchange $J \approx 15-20$ meV, (ii) vastly different for “up” and “down” Ni spins (assuming $\theta = 35^\circ$ we get between the two a factor of $3 \times 10^{-4}$), and (iii) effective down to very low frequencies, $\sim \gamma$. Coming to the Fe-NiO data, we can now attribute the experimental dissipation of about 35 meV of the $\downarrow$-polarized tip oscillating over a $\downarrow$ Ni spin to nonmagnetic mechanisms, that of about 50 meV over an $\uparrow$ Ni in terms of the same mechanism plus a hysteretic magnetic dissipation $W \approx 15$ meV, implying that the tip-surface coupling resulted in $\alpha > 1$.

The strong dependence of that coupling on $f_{\text{ex}}$ allows in principle for a reduction of $\alpha$ and a phase transition from overdamped to underdamped. In that case we would expect the faster evolution timescale to suppress the hysteretic behavior, dramatically reducing the magnetic dissipation.

\[ \text{References} \]

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