Merkle-CRDTs
Merkle-DAGs meet CRDTs

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Abstract—We study Merkle-DAGs as a transport and persistence layer for Conflict-Free Replicated Data Types (CRDTs), coining the term Merkle-CRDTs and providing an overview of the different concepts, properties, advantages and limitations involved. We show how Merkle-DAGs can act as logical clocks giving Merkle-CRDTs the potential to greatly simplify the design and implementation of convergent data types in systems with weak messaging layer guarantees and a very large number of replicas. Merkle-CRDTs can leverage highly scalable distributed technologies like DHTs and PubSub algorithms running underneath to take advantage of the security and de-duplication properties of content-addressing. Examples of such content-oriented systems could include peer-to-peer content exchange and synchronisation applications between opportunistically connected mobile devices, IoT devices or user applications running in a web browser.

I. INTRODUCTION

The advent of blockchain technology has generalized the use of peer-to-peer networking along with cryptographically-directed acyclic graphs, known as Merkle-DAGs, to implement globally distributed and eventually consistent data structures in applications such as cryptocurrencies. In these systems, the Merkle-DAG is a content-addressed data structure used to provide both causality information and self-verification of objects that can be easily and efficiently shared in trustless peer-to-peer environments. The need to maintain and apply certain rules to add new blocks to the blockchains in adversarial scenarios usually warrants the use of consensus algorithms.

A different approach to obtaining eventual consistency in a distributed system is by using Conflict-Free Replicated Data Types (CRDTs) [28], [31]. CRDTs are useful in non-adversarial scenarios, where the participating replicas are known to behave correctly. CRDTs rely on some properties of the data objects themselves that enable convergence towards a global, unique state without the need for consensus. CRDTs come in two main flavours: state-based CRDT [4]—where the states of replicas form a join-semilattice and are merged under the guarantees afforded by it—and operation-based CRDT [4]—in which commutative operations are broadcast and applied to the local state by every replica. Additionally, δ-CRDTs are an optimization of state-based CRDTs to reduce the size of the payloads sent by the replicas.

Both Merkle-DAGs and CRDTs provide interesting properties: the former allows distributed systems to take advantage of a content-addressing layer for the resolution/discoverability and self-verification of data regardless of the source location; the latter allows global state convergence without the need for—usually complex and expensive—consensus mechanisms. By embedding CRDT objects inside Merkle-DAG nodes, we obtain the best properties of both worlds, that is, we obtain a convergent system that can leverage the DAG as a logical clock. This logical clock is provided and built by every replica without the need for coordination. Replicas can operate undisrupted in loose network environments with no delivery guarantees. As we will see, a system based on Merkle-CRDTs is fully agnostic to how the system announces and discovers data among replicas, thus being able to leverage different approaches like those provided by DHT and PubSub mechanisms without being tied to a particular version of them. This is in stark contrast to traditional consensus algorithms, e.g., Raft, which are tied to particular message dissemination protocols.

We conceive this approach as extremely useful for fully distributed and unstructured peer-to-peer applications, where the replicas are writers to a common dataset, usually in the form of a database. This is the case for example, in a distributed and fully replicated file-system, chat group or package repository index. We have found that using the InterPlanetary File System (IPFS) [14] (see Section II-F) as a content-addressed, peer-to-peer decentralised file system and content distribution network, a Merkle-CRDT-based system scales well to the order of thousands of replicas which can opportunistically join and depart – a very common condition when working with mobile, browsers or IoT devices.

The InterPlanetary File System provides a content-addressed peer-to-peer filesystem [14], which supports seamless syncing of Merkle-DAGs with arbitrary formats and payloads, making it a robust building block for different types of distributed applications like PeerPad [4] or OrbitDB [4], both powered by CRDTs and IPFS. IPFS not only delivers the right environment for working with content addressed data (like the Merkle-DAG that we will use), but also allows our CRDT application to be fully detached from the lower layers of the distributed system: networking transports, discovery and data transfer facilities come in modules which can be swapped and tweaked independently. Leveraging such system greatly simplifies the design and optimization of the CRDT layer so

¹Also known as Convergent CRDTs or CvRDTs.
²Also known as Commutative CRDTs or CmRDTs.
³PeerPad is a real time p2p collaborative editing tool (https://peerpad.net).
⁴OrbitDB is a peer-to-peer database for the decentralized web (https://github.com/orbitdb/orbit-db).
that it adapts well to the use case it is meant to serve.

In this paper we formalize what we refer to as Merkle-CRDTs. The goal is to provide an overview of their properties, advantages and limitations, so that it can set the ground layer for future research and optimizations in the space. For example, Merkle-CRDTs allow building fully distributed key-value stores in real-world systems in networks with no message delivery guarantees and fully flexible replica sets that can grow and shrink at any time without impacting the CRDT layer.

The contributions of this paper are as follows:

- We define Merkle-Clocks as Merke-DAG-based logical clocks, to represent causality information in a distributed system. Embedding causality information using Merkle-DAGs is at the core of cryptocurrencies and source control systems like Git but they are rarely considered separately as a type of logical clock. We demonstrate that Merkle-Clocks can be used in place of other logical clocks traditionally used by CRDTs like version vectors and vector clocks. We show that Merkle-Clocks can, in fact, be seen as CRDT objects themselves, which can be synced and merged and for which we can formally prove eventual consistency across different replicas.

- We define Merkle-CRDTs as a general purpose transport and persistence layer for CRDT payloads which leverages the properties of Merkle-Clocks, using the DAG-Syncer and the Broadcaster to provide per-object causal consistency by design. This enables the use of simple CRDT types in systems with weak messaging layer guarantees and large number of replicas.

Our intention with this paper is to show that eventual consistency between replicas can be achieved independently of the underlying transport mechanisms and in a setting where all peers are equal. This means that Merkle-CRDTs can be implemented on top of any underlying peer discovery and routing system (e.g., DHT, PubSub). We argue that this is a very powerful concept that has the potential to lead to new eventual consistency system designs. It is also fundamentally different to traditional consensus algorithms, such as Raft, where at any given time there needs to be a leader peer that collects the latest state from all other peers. As such, we do not provide an evaluation against these traditional approaches as their requirements and design principles are fundamentally different.

The rest of the paper is organised as follows: In Section II we start by introducing relevant background concepts and prior art. In Section III we expose the characteristics of our system model and introduce the facilities needed to store and sync Merkle-CRDTs.

In Section IV we introduce Merkle-Clocks and, building on the previous sections, in Section V we define Merkle-CRDTs. We discuss how different CRDT payloads (whether operation-based, state-based or δ-based) benefit from Merkle-CRDTs. Finally, we describe some of the limitations and inefficiencies of Merkle-CRDTs and introduce techniques to overcome them in Section VI.

## II. BACKGROUND & RELATED WORK

### A. Eventual consistency

**Eventual Consistency** (EC) in distributed systems refers to the situation where the state may not be the same across replicas of the system but, given enough time and perhaps after network partitions, downtime and other eventualities have been resolved, the system design will ensure that the state becomes the same everywhere.

The main weakness of the eventual consistency definition is that it offers no guarantees as to when the shared state will converge or how much the individual states will be allowed to diverge until the first strong eventual consistency (SEC) addresses these issues by establishing an additional safety guarantee: if two replicas have received the same updates, their state will be the same.

Consensus algorithms or, more important to this paper, Conflict-Free Replicated Data Types (CRDTs) are ways to achieve (strong) eventual consistency in a distributed system.

### B. Merkle DAGs

A Directed Acyclic Graph (DAG) is a type of graph in which edges have direction and cycles are not allowed. A Merkle-DAG is a DAG where each node has an identifier and this is the result of hashing the node’s contents. Identifying a data object (like a Merkle-DAG node) by the value of its hash is referred to as content addressing (e.g., $A = Hash(B) \rightarrow B = Hash(C) \rightarrow C = Hash(\emptyset)$). Thus, we name the node identifier as Content Identifier or CID.

Merkle-DAGs are self-verified and immutable structures. The CID of a node is univocally linked to the contents of its payload and those of all its descendants. Thus two nodes with the same CID univocally represent exactly the same DAG. This will be a key property to efficiently sync Merkle-CRDTs without having to copy the full DAG, as exploited by systems like IPFS.

Merkle-DAGs are widely used. Source control systems like Git use them to efficiently store the repository history in a way that enables de-duplicating the objects and detecting conflicts between branches. In distributed databases like Dynamo, Merkle-Trees are used for efficient comparison and reconciliation of the state between replicas. In Hash Histories, content addressing is used to refer to a Merkle-Tree representing a state.

Merkle-DAGs are also the foundational block of blockchains—they can be seen as a Merkle-DAG with a single branch—and their most common application: cryptocurrencies (e.g., Bitcoin). Cryptocurrencies like Bitcoin benefit from the embedded causality information encoded in the chain: transactions in a block deeper in the chain always happened before those of earlier blocks. One of the main issues in cryptocurrencies is to make all participating peers agree about the tip/head/root of the chain.

One commonality in many of these systems is that the Merkle-DAG implicitly embeds causality information. The

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3 EC only provides a liveness guarantee: the system will not become stuck when making progress to converge.
DAG can show that a certain transaction precedes another or that a Git commit needs to be merged rather than fast-forwarded. This will be one of the properties that we use in Merkle-CRDTs and that this paper makes explicit and puts in contrast with other causality-encoding mechanisms known as logical clocks.

C. Logical clocks

The design of causally-convergent systems involves the reconciliation of diverging state versions among different replicas when, for example, events occur concurrently.

*Logical clocks* are the alternative to global time, which has traditionally proved difficult to realise in distributed systems. They provide ways to encode causal information between events known to different actors in a distributed system.

Logical clocks are representations of causal histories and provide a partial ordering between events. That is, given two events a and b, logical clocks should be able to tell us if a happened before b (a → b), or vice-versa (b → a), or if both a and b happened concurrently (a || b).

The practical implementation of logical clocks usually involves metadata which travels attached to every event in the system. One of the most common forms of logical clocks are version vectors: every replica maintains and broadcasts a vector that tracks on which version the state of all the replicas is. When a replica performs a modification of the state, it increases its version. When a replica merges a state from a different replica, it takes the highest between the local versions and the versions provided by the other replica along with the event. Thus, given two events a, b, with version vectors V^a, V^b: a → b if V^a_i ≤ V^b_i for each position i in the vectors. If a ∇ b and b ∇ a, by that definition, a and b are concurrent.

In this paper we demonstrate that a Merkle-DAG can act as a logical clock. Merkle-Clocks, as we will show, provide a different set of properties but encode the same causal information about events.

D. Conflict-Free Replicated Data Types (CRDTs)

CRDTs are data types which provide strong eventual consistency among different replicas in a distributed system by requiring certain properties from the state and/or the operations that modify it. Additionally, CRDTs also feature monotonicity. The concept of monotonicity applied to data types is the notion that every update is an inflation, making the state grow, not in size, but in respect to a previous state. This implies that there will always be an order between states. Monotonicity implies that rollbacks on the state are not necessary regardless of the order in which updates happen.

There are two prominent types of CRDTs: state-based and operation-based CRDTs. In state-based CRDTs, all the states in the system—that is, the states in different replicas and different moments—form a monotonic join-semilattice. That means that, for any two states X and Y, both can be "joined" (merged, or form a union) (⊔) and the result is a new state corresponding to the Least-Upper-Bound (LUB) of the two. In other words, every modification made to a state by a replica must be an inflation and the union of two states X and Y is the minimal state capable of containing both X and Y and not more (the LUB). A join-semilattice is thus a partially ordered set and its LUB is the smallest state capable of containing all the states in the semilattice. This implies that the ⊔ operation must be idempotent (X ⊔ X = X), commutative (X ⊔ Y = Y ⊔ X) and associative ((X ⊔ Y) ⊔ Z = X ⊔ (Y ⊔ Z)).

Replicas in a state-based CRDT modify their state—or inflate it—and broadcast the resulting state to the rest of replicas. Upon receiving the state, the other replicas merge it with the local state. The properties of the state ensure that, if the replicas have correctly received the states sent by other replicas—and vice-versa—they will eventually converge.

Operation-based CRDTs, on the other side, do not enforce any property on the state itself but on the operations used to modify it, which must be commutative (at least with regard to a different operation issued at the same time concurrently). The replicas broadcast the operations and not the states. If two operations happen at the same time in two replicas, the order in which other replicas apply them does not matter: the resulting states will be the same.

It follows that, if an operation broadcast does not arrive to a replica—for example due to a network failure—that replica will never be able to apply it and the states will not converge. Thus, unlike state-based CRDTs, eventual consistency in operation-based CRDTs requires a reliable messaging layer that eventually delivers all operations. Additional constraints may be necessary, for example, if operations are not idempotent: in that case, the messaging layer should ensure that each operation is delivered exactly once.

Logical clocks, as seen in the previous section, are commonly used to implement CRDT types: they are useful to identify when two updates happen concurrently and need merging. CRDTs have been successfully used and optimized in different applications and distributed databases, Basho’s Riak being one of the most prominent examples.

E. Sync Protocols in Information-Centric Networks

There are multiple types of logical clocks that are similar to version vectors discussed earlier, but fulfill different needs or address some of their shortcomings: vector clocks, bounded version vectors, dotted version vectors, tree clocks or interval tree clocks are some of them.

There has been a recent body of work in distributed dataset synchronisation in the area of Information-Centric Networks (ICN). Information-Centric architectures are advocating direct content naming at the network layer and subsequent routing and forwarding (by core network routers), based on content names and (in some cases) longest-prefix matching.

ChronoSync is utilising the features of the Named-Data Networking architecture to synchronise state between different datasets. ChronoSync is a data-layer mechanism, which, however, takes advantage of the hierarchical and flexible naming scheme that NDN is building on. Inspired
by Merkle Trees, ChronoSync is using cryptographic digests and filters to synchronise datasets between peers. ChronoSync takes advantage of the name-based nature of the underlying network (NDN) and is assigning a unique publishing prefix to each peer. This unique prefix, together with sequence numbers and network layer persisting/long-lived “Interest packets” is replacing much of what other approaches attempt to do with clocks and CRDTs. While integrating sync functionality at the network layer allows for more native designs, some features are inevitably lost. For example, ChronoSync cannot deal with simultaneous (concurrent) data publication. RoundSync \cite{30} is partially solving this problem by splitting the synchronisation process in rounds.

VectorSync \cite{29} is an enhanced version of ChronoSync which uses version vectors to make synchronisation between peers more efficient. Version vectors are more efficient in detection of inconsistencies, than simple message digests, as mentioned earlier. However, similarly to other proposals in the area, VectorSync needs to realise a ‘leader-based membership management’ in order to deal with active members that update the state of the dataset.

The integration of distributed dataset synchronisation features natively at the network layer of the network is clearly an advanced endeavour, which comes with its own challenges. We believe that the advantage of “transport-agnostic” state synchronisation brought by Merkle-CRDTs can apply and improve the performance of protocols such as ChronoSync, RoundSync or VectorSync. On the other hand, handling Merkle-CRDT-based state synchronisation directly through named network objects brings standard ICN advantages to Merkle-CRDTs. As such we consider those two distinct approaches to state synchronisation as complementary.

F. IPFS: The InterPlanetary File System

IPFS \cite{14} is a content-addressed, distributed filesystem. It uses a Distributed Hash Table (DHT) to announce and discover which replicas (or peers) provide certain Merkle-DAG nodes. It implements a node-exchange protocol called bitswap to retrieve DAG nodes from any provider. IPFS is built on top of libp2p \cite{5}, a modular network protocol stack for P2P networks, which additionally provides efficient broadcasting mechanisms primarily based on publish-subscribe models \cite{2}.

IPFS also uses IPLD, the InterPlanetary Linked Data Format \cite{4}, a framework to describe Merkle-DAGs with arbitrary node formats and support for multiple types of CIDs \cite{6}, making it very easy to create and sync custom DAG nodes.

These features make IPFS a suitable layer on which to implement Merkle-CRDTs, as it provides the necessary mechanisms to discover, route and announce content in potentially very large networks. This is not to say that other transport mechanisms are not suitable to build Merkle-CRDTs on top.

We assume the presence of an asynchronous messaging layer which provides a communication channel between separate replicas. This channel is managed by two facilities which every replica exploits: the DAG-Syncer and the Broadcaster components (defined below).

We assume that messages can be dropped, reordered, corrupted or duplicated. It is not necessary to know beforehand the number of replicas participating in the system. Replicas can join and leave at will, without informing any other replica. There can be network partitions but they are resolved as soon as connectivity is re-established and a replica broadcasts a new event.

Replicas may have durable storage, depending on their own requirements and data types. Using Merkle-CRDTs, new replicas and crashed replicas without durable storage will be able to eventually re-construct the complete state of the system as long as at least one other replica is in the latest system state.

A. The DAG-Syncer component

A DAG-Syncer is a component that enables a replica to obtain remote Merkle-DAG nodes from other replicas given their content identifiers (CIDs) and to make its own nodes available to other replicas. Since a node contains links to their direct descendants, given the root node’s CID, the DAG-Syncer component can be used to fetch the full DAG by following the links to children in each node. Thus, we can define the DAG-Syncer as follows:

Definition 1. (DAG-Syncer). A DAG-Syncer is a component with two methods:

- Get (CID) : Node
- Put (Node)

We do not specify any more details such as how the protocol to announce and retrieve nodes looks like. Ideally, the DAG-Syncer layer should not impose any additional constraints on the system model. Our approach relies on the properties of the DAG-Syncer and Merkle-DAGs to tolerate all the network contingencies described above.

B. The Broadcaster component

A Broadcaster is a component to distribute arbitrary data from one replica to all others (directly or through relays). Ideally, the payload will reach every replica in the system, but this is not a requirement for every broadcast message:

Definition 2. (Broadcaster). A Broadcaster is a component with one method:

- Broadcast (Data)

C. IPFS as a DAG-Syncer and Broadcaster component

The components above can be realised by using IPFS (as introduced in Section III). IPFS can act as the DAG-Syncer, while one of the PubSub mechanisms provided by its libp2p layer can perform the tasks of the Broadcaster component.

Such an implementation should allow extreme scalability of the replica set in general. The peers in the network do not need to be fully connected to everyone else and the system is extremely modular and configurable to fit both small
devices and large storage servers. The choice of settings and implementations will affect the performance of the system under different circumstances and network topologies but is independent from the Merkle-CRDT objects and datatype.

IV. MERKLE-CLOCKS

A. Overview

A Merkle-Clock $\mathcal{M}$ is a Merkle-DAG where each node represents an event. In other words, given an event in the system, we can find a node in this DAG that represents it and that allows us to compare it to other events.

The DAG is built by merging other DAGs (those in other replicas) according to some simple rules. New events are added as new root nodes (parents to the existing ones). Note that the Merkle-Clock may have several roots at a given time.

For example, given $\mathcal{M}_\alpha$ and $\mathcal{M}_\beta$ ($\alpha$ and $\beta$ being the single root CIDs in those DAGs):  

1) If $\alpha = \beta$ no action is needed, as they are the same DAG.
2) else if $\alpha \in \mathcal{M}_\beta$, we keep $\mathcal{M}_\beta$ as our new Clock, since the history in $\mathcal{M}_\alpha$ is part of it already. We say that $\mathcal{M}_\alpha < \mathcal{M}_\beta$ in this case.
3) else if $\beta \in \mathcal{M}_\alpha$, we keep $\mathcal{M}_\alpha$ for the same reason. We say that $\mathcal{M}_\beta < \mathcal{M}_\alpha$ in this case.
4) else, we merge both Clocks by keeping both DAGs as they are and thus having two root nodes, those referenced by $\alpha$ and $\beta$. Note that $\mathcal{M}_\alpha$ and $\mathcal{M}_\beta$ could be fully disjoint or not, depending on whether they share some of their deeper nodes. If we wish to record a new event, we can create a new root node with two children, $\alpha$ and $\beta$.

We can already see that, by determining if one Merkle-Clock is included in another, we are introducing the notion of order among Merkle-Clocks. In the same way, we have a notion of order among the nodes in each clock, since events that happened earlier will always be descendants of events that happened later. Additionally, we have introduced a way to merge Merkle-Clocks according to how they compare. The resulting Merkle-Clock always includes the causality information from both Merkle-Clocks. This eventually means that the causality information stored in Merkle-Clocks in every replica will converge to the same Merkle-Clock after merging.

The causal order provided by Merkle-Clocks is embedded when building Merkle-DAGs with similar rules and usually overlooked as something very intuitive. It is important, however, to formalize how we define order between Merkle-Clocks and to prove that the causality information is maintained when they are synced and merged. This is the subject of the next section and will be an important property for Merkle-CRDTs.

B. Merkle-Clocks as a convergent, replicated data type

This section formalizes the definition of Merkle-Clocks and their representation as Merkle-Clock DAGs. We will show that Merkle-Clock DAGs can be seen as a Growing-Set (G-Set) CRDT and therefore converge in multiple replicas.

Let $\mathcal{E}$ be the set of all system events:

Definition 3. (Merkle-Clock Node). A Merkle-Clock Node $n_{\alpha}$ is a triple:

$$(\alpha, e_{\alpha}, C_{\alpha})$$

which represents an event $e_{\alpha} \in \mathcal{E}$, with $\alpha$ being the node CID and $C_{\alpha}$ being the CID-set of $n_{\alpha}$’s direct descendants.

Definition 4. (Merkle-Clock DAG). A Merkle-Clock DAG is a pair:

$$\langle N, \leq \rangle$$

where $N$ is a set of immutable DAG-nodes and a partial order $\leq$ on $N$, defined as follows:

$$n_{\alpha}, n_{\beta} \in N : n_{\alpha} < n_{\beta} \iff n_{\alpha} \text{ is a descendant of } n_{\beta}$$

In other words, $n_{\alpha} < n_{\beta}$ if there is a path of linked nodes which goes from $n_{\beta}$ to $n_{\alpha}$.

In order to maintain this relationship, the Merkle-Clock DAG must be built with the following Implementation Rule: 

IR. Every new event in the system must be represented as a new root node to the existing Merkle-Clock DAG(s). In particular, the $C$ set must contain the CIDs of the previous roots.

Definition 5. (Merkle-Clock). A Merkle-Clock ($\mathcal{M}$) is a function which given an event $e_{\alpha} \in \mathcal{E}$ returns a node from the Merkle-Clock DAG $N$:

$$\mathcal{M} : \mathcal{E} \rightarrow N$$

Remark. A Merkle-Clock satisfies the Strong Clock condition [22]. We see that every node represents a later event than that of its children:

$$\forall (\beta, e_{\beta}, C_{\beta}) \in N : \forall \alpha \in C_{\beta} : e_{\alpha} \rightarrow e_{\beta}$$

Since every event is the root of a (sub)DAG built using the implementation rule, we can immediately see that earlier Merkle-Clock values are descendants of the later ones:

$$\mathcal{M}(e_{\alpha}) < \mathcal{M}(e_{\beta}) \iff e_{\alpha} \rightarrow e_{\beta}$$

We can now define a join-semilattice of Merkle-Clocks DAGs as a pair:

$$\langle J, \subseteq_J \rangle$$

where $J$ is a set of Merkle-Clocks DAGs $\subseteq_J$ a partial order over that set defined as follows. Given $M, N \in J$:

$$M \subseteq J N \iff \forall m \in M, \exists n \in N \mid m < n \Rightarrow M \subseteq N$$

Note that $m < n$, means that $m$ is a descendant of $n$ and thus must belong to the same DAG, then $\subseteq_J$ simply means that $M$ is a subset of $N$.

This allows us to define the Least-Upper-Bound of two Merkle-Clocks DAGs ($\bigcup_J$) as the regular union of the sets:

$$M \bigcup_J N = M \cup N$$

Unsurprisingly, the Merkle-Clock representation corresponds in fact to a Grow-Only-Set (G-Set) in the state-based CRDT form [31]. The elements of the set are immutable, cryptographically linked and represent the events in the system.

In the next section we will see how the properties of Merkle-DAGs allow syncing Merkle-Clocks in a more efficient manner than regular state-based G-Sets.
C. The Merkle in the Clocks: properties of Merkle-Clocks

We have so far defined a way to encode causality information per replica and ensured that two replicas can merge their Merkle-Clocks. Now we will see how the properties of Merkle-DAGs allow the use of a pull rather than a push approach which, together with content-addressing, enables efficient clock sync between replicas and overcomes the effect of network partitions or contingencies. The steps to Merkle-Clock synchronisation between replicas are given below.

1) Broadcasting the Merkle-Clock requires broadcasting only the current root CID. The whole Clock is unambiguously identified by the CID of its root and its full DAG can be walked down from it as needed.

2) The immutable nature of a Merkle-DAG allows every other replica to perform quick comparisons and pull/fetch only those nodes that it does not already have.

3) Merkle-DAG nodes are self-verified, through their CID, and, therefore, immune to corruption and tampering. Hence, they can be fetched (pulled) from any source willing to provide them, trusted or not.

4) Identical nodes are de-duplicated by design: there can only be one unique representation for every event.

In practice, every replica just fetches the delta causal histories from other replicas without the need to build those deltas explicitly anywhere in the system. A completely new replica with no previous history will fetch the full history automatically.8

Merkle-Clocks can replace version clocks and other logical clocks that are usually part of CRDTs. This comes with some considerations:

- By using Merkle-Clocks we can decouple the causality information from the number of replicas, which is a common limitation in version clocks. This makes it possible to reduce the size of the messages when implementing CRDTs and, most importantly, solves the problem of keeping clocks working when replicas randomly join and leave the system.

- On the downside, the causal information grows with every event and replicas store potentially large histories even if the event information is consolidated into smaller objects.

- Keeping the whole causal history enables new replicas to sync events from scratch out-of-the-box, without having to explicitly send system snapshots to newcomers. However, that syncing may be slow if the history is very large. We will explore, along with Merkle-CRDTs, potential optimizations in this regard.

A significant advantage of Merkle-Clocks over traditional version clocks is that they can also deal with several types of network anomalies:

- Dropped messages may prevent other replicas from learning about new roots. But since every Merkle-Clock DAG is superseded by future DAGs and every download fetches all the missing parts of a DAG, network partitions and replica downtimes do not have an effect on the overall system and will begin to heal automatically once the issues are resolved.

- Out of order delivery poses no problem for the same reasons. The missing DAG will be fetched and processed in order.

- Duplicated messages are just ignored by replicas as they are already incorporated into their Merkle-Clocks.

- Corrupt messages come in two forms: a) if the message broadcasting a new root is corrupted, then it will be a hash corresponding to a non-existent DAG that cannot be fetched by the DAG-Syncer and will be eventually ignored; b) if a DAG node is corrupted on download, the DAG-Syncer component (or the application) can discard it if its CID does not match the downloaded content.

As we showed in the previous section, Merkle-Clocks represent a strict partial order of events. Not all events in the system can be compared and ordered. For example, when having multiple roots, the Merkle-Clock cannot say which of the events happened first.

A total order can be useful and could be obtained, for example, by considering concurrent events to be equal. Similarly, a strict total order could be built by sorting concurrent events by the CID of their nodes or by any other arbitrary user-defined strategy based on additional information attached to the clock nodes. Any such approach would qualify as data-layer conflict resolution.

V. MERKLE-CRDTs: MERKLE-CLOCKS WITH PAYLOAD

Definition 6. (Merkle-CRDT). A Merkle-CRDT is a Merkle-Clock whose nodes carry an arbitrary CRDT payload.

Merkle-CRDTs keep all the properties seen before for Merkle-Clocks. However, for the payloads to converge, they need to be convergent data types (CRDTs) themselves. The advantage is that Merkle-Clocks already embed ordering and causality information which would otherwise need to travel embedded in the CRDT objects (usually in the form of other logical clocks), or be provided by a reliable messaging layer.

Thus, the implementation of a Merkle-CRDT node is:

\[(\alpha, P, C)\]

with \(\alpha\) being the content identifier, \(P\) an opaque data object with CRDT properties and \(C\) the set of children identifiers.

A. Per-object causal consistency and gap detection

The directed-link nature of Merkle-CRDTs, which allows traversing the full causal history of the system in the order of events, provides all the necessary properties to ensure per-object causal consistency and gap detection by design without modifying our system model.

This means that Merkle-CRDTs are very well suited to carry operation-based CRDTs as they can ensure that no operation is lost or applied in disorder.9

8This is how peers participating in cryptocurrency mining sync their ledgers.9Recall that the Merkle-Clock provides a strict partial order of events. In this case, two non-concurrent operations applied to an object will be sortable by the clock.
To facilitate the task of processing CRDT payloads in Merkle-CRDTs, in the next section we present a general and simple (non-optimized) anti-entropy algorithm that can be used to obtain per-object causal consistency for any CRDT embedded object.

B. General anti-entropy algorithm for Merkle-CRDTs

Definition 7. (General anti-entropy algorithm for Merkle-CRDTs).

Let $\mathcal{R}^A$ and $\mathcal{R}^B$ be two replicas using Merkle-CRDTs with $\mathcal{M}_\alpha$ and $\mathcal{M}_\beta$ respectively as their current Merkle-CRDT DAG.

1) $\mathcal{R}^B$ issues a new payload by creating a new DAG node $(\beta, P, \{\theta\})$ and adding it as the new root to its Merkle-CRDT, which becomes $\mathcal{M}_\beta$.

2) $\mathcal{R}^B$ broadcasts $\beta$ to the rest of replicas in the system.

3) $\mathcal{R}^A$ receives the broadcast of $\beta$ and retrieves the full $\mathcal{M}_\beta$. It does this by starting from the root $\beta$ and walking down the DAG using the DAG-Syncer component to fetch all the nodes that are not in $\mathcal{M}_\alpha$, while collecting their CIDs in a CID-Set $\mathcal{D}$. Given the inherent properties of DAGs, for any CID already in $\mathcal{M}_\alpha$ the whole sub-DAG can be skipped.

4) If $\mathcal{D}$ is empty, no further action is required. $\mathcal{R}^A$ must have already processed all the payloads in $\mathcal{M}_\beta$. This means that $\mathcal{M}_\beta \subseteq \mathcal{M}_\alpha$.

5) If $\mathcal{D}$ is not empty, we sort the CIDs in $\mathcal{D}$ using the order provided by the Merkle-Clock. We can skip the ordering if causal delivery is not a requirement in our system. The amount of items in $\mathcal{D}$ will depend on the amount of concurrency in the system and how long the two Merkle-CRDTs have been allowed to diverge, but should be small under normal circumstances.

6) $\mathcal{R}^A$ processes the payloads associated with the nodes corresponding to the CIDs in $\mathcal{D}$, from the lowest to the highest.

7) If $\alpha \in \mathcal{D}$, then $\mathcal{M}_\alpha \subseteq \mathcal{M}_\beta$ and $\mathcal{M}_\beta$ becomes the new local Merkle-CRDT in $\mathcal{R}^A$.

8) else, $\mathcal{M}_\alpha \not\subseteq \mathcal{M}_\beta$ and $\mathcal{M}_\beta \not\subseteq \mathcal{M}_\alpha$. $\mathcal{R}^A$ keeps both nodes as roots.

C. Operation-based Merkle-CRDTs

Definition 8. Operation-based Merkle-CRDTs are those in which nodes embed an operation-based CRDT payload.

Operation-based Merkle-CRDTs are the most natural application of Merkle-CRDTs. Operations are easy to define, as they just need to be commutative, so that the resulting state will be the same in every replica regardless of the order in which they have received the operations. However, that also means that for states to converge, every operation must be received. A reliable messaging layer [11] is then a prerequisite for convergence, but in real world networks with a large number of replicas it is usually not possible to ensure that no message is lost. This leaves us with complex workarounds, like additional causality payloads, buffering and retry mechanisms that must accompany the CRDT implementation, turning what should be a simple CRDT implementation into something considerably more complicated.

Merkle-DAGs provide all the properties of a messaging layer where messages are always delivered in order, verified and never repeated nor dropped. Thus, Merkle-CRDTs enable operation-based CRDTs in contexts where they could not be easily used before.

As we saw, thanks to the Merkle-DAG in which they are embedded, each replica only needs the missing parts of the DAG and these can be fetched once the root is known. This includes new replicas joining the system, which will be able to fetch and apply all operations. We do not need to keep knowledge of the full replica set and place the responsibility of efficient broadcast in the Broadcaster component.

D. State-based Merkle-CRDTs

Definition 9. State-based Merkle-CRDTs are those in which nodes embed a state-based CRDT payload.

Embedding full states in each Merkle-CRDT node is counter-intuitive since state-based CRDTs already provide per-object causal consistency and can cope with unreliable message layers by design.

Moreover, although the final state would result from the merge of all the states in the Merkle-CRDT nodes, the DAG-Syncer component would still need to store those states, something prohibitive when working with large state objects. That said, Merkle-CRDTs remove the need to attach causality metadata and detach it from the number of replicas, which might be of interest for state-based CRDTs with very small states in comparison to the number of replicas.

A more interesting approach is that of $\delta$-CRDTs [10] which, instead of broadcasting full states, are able to send smaller sections (deltas). $\delta$-mutations, as these objects are called, can be merged downstream just like any full state would be, without the need for changing the semantics of the $\text{union}$ operation. It follows that multiple deltas can be merged to form what is known as $\delta$-groups and increase the efficiency of the broadcast payloads. As pointed out in [10], “a full state can be seen as a special (extreme) of a delta-group”.

In the vanilla form of $\delta$-CRDTs, however, consistency is delayed ad-infinum when a message is lost and the per-object causal consistency property of state-based CRDTs is lost. These issues can be addressed with an additional anti-entropy algorithm that groups, sorts, tracks delivery and re-sends missing deltas, as presented in [10], but in the case of $\delta$-state-Merkle-CRDTs, the anti-entropy algorithm and any causal information attached to the original objects would not be necessary. In essence, this approach brings $\delta$-state Merkle-CRDTs closer to their operation-based counterpart.

VI. LIMITS AND OPTIMIZATIONS OF MERKLE-CRDTs

A. Limitations of Merkle-CRDTs

We have so far focused on explaining the different qualities that Merkle-CRDTs provide when compared to traditional CRDT approaches, but we must also highlight what intrinsic and practical limitations they bring.
a) Ever-growing DAG-Size: The most obvious consequence of Merkle-CRDTs is that, while CRDTs normally merge, apply, consolidate and discard broadcast objects, Merkle-CRDTs build a permanent Merkle-DAG which must be stored and is ever-growing. As we have seen, this provides a number of advantageous properties, but also comes with some implications:

- The size of the DAG might grow larger than acceptable. The rate of growth will depend on the number of the events and the size of the payloads. This is very similar to how blockchains grow to large sizes in time. In some cases, it might be possible to express the state as a compact of the result of all the Merkle-CRDT operations, but this brings us to the next point.
- If replicas store the Merkle-DAG only, knowing that the full state can be rebuilt from it (and thus saving that space), starting replicas with very large Merkle-DAGs might be especially slow since they will need to reprocess the full DAG, even when available locally. If not, there will be redundant information stored in both the resulting state and in the Merkle-DAG.
- Merkle-CRDT syncs from scratch are possible and natural to the system when a new replica joins. However, Merkle-DAGs are not only ever-growing but also tend to be deep and Thin. A new replica will learn the root CID from a broadcast operation and will need to resolve the full DAG from it. Because of the thinness, it will not be possible to fetch several branches in parallel. Cold-syncs may take significantly longer than it would take to ship a snapshot, thus rendering the embedded property of Merkle-DAGs of little value.

Very large DAGs and slow syncs are not a problem in some scenarios and can be seen as an acceptable trade-off, but do highlight the need of exploring “garbage collection” and DAG compaction mechanisms.

b) Merkle-Clock sorting: Merging two Merkle-Clocks requires comparing them to see if they are included in one another and finding differences. This may be a costly operation if DAGs have diverged significantly (or long ago).

c) DAG-Syncer latency: Replicas rely on a DAG-Syncer component to fetch and provide nodes from and to the messaging layer. As mentioned earlier, Merkle-CRDTs are agnostic to the mechanism used to synchronise messages (e.g., DHT or PubSub), but unless chosen carefully, this mechanism might introduce sync delay. Depending on application requirements, this delay might or might not be acceptable.

The practical impact of these limitations depends on the requirements of the application. In particular, when thinking about adopting Merkle-CRDTs, users should consider whether Merkle-CRDTs are the best approach in terms of: i) Node count vs, state-size, ii) Time to cold-sync, iii) Update propagation latency, iv) Expected total number of replicas, v) Expected replica-set modifications (joins and departures), vi) Expected volume of concurrent events.

B. Optimizing Merkle-CRDTs

a) Delayed DAG nodes: In scenarios where replicas issue frequent updates, we can group multiple payloads before issuing a single node containing all of them. It is clear that this approach will bring some benefits, which however, comes with trade-offs: updates are not immediately sent out and will, therefore, take longer to propagate.

b) Quick Merkle-DAG inclusion check: Merging the local replica DAGs with a remote one requires checking if one DAG includes the other. It is possible but inefficient to do so by walking down the first DAG looking for a node CID that matches the root of the second. Storing the CID of the local DAG in a key-value store that can quickly check whether a CID is part of the local DAG or not makes things significantly easier. When walking the remote DAG to check for inclusion of the local DAG, the CIDs of the children of any of its nodes can be checked to see if they are part of the local DAG in which case their branches can be conveniently pruned. This implies, however, that the implementation must be aware and have access to the local storage system for nodes. The DAG-Syncer, as currently defined, cannot differentiate between nodes available locally or remotely. Bloom filters, caches and some data structures can also improve efficiency, but they are usually part of the chosen storage backend.

A similar effect can be achieved by embedding version vectors in the payloads, as long as the application can tolerate the constraints they impose. Comparing version vectors between payloads is an inclusion check without the need to perform a DAG-walking.

c) Broadcast payload adjustments: Our standard approach reduces the size of the broadcasts by including only the CID of the new roots. Publishing mechanisms are complex enough and always benefit from smaller payloads.

d) Reducing the Merkle-DAG node size: We can attempt to reduce the size of the payloads as much as possible by compressing and removing redundant information not required by the CRDT itself. For example, instead of signing the CRDT payloads to ensure that they come from a trusted replica, we can sign the broadcast messages, thus leaving signatures out of the Merkle-DAG.

e) Additional pointers in nodes: One of the ways to work around the thin-DAG problem is to regularly introduce references to deeper parts of the DAG when issuing new nodes. This method is basically adding extra children to nodes. It allows more parallelism when fetching missing parts of the DAG by being able to jump to other sections of it, resulting in much faster traversals. The actual number of extra links and their destination will depend on the needs of the application.

The above recommendations should be considered in any Merkle-CRDT implementation as they can provide significant advantages over the un-optimized version described previously. Which optimizations fit to which implementation is largely

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10] Bitcoin chain uses more than 220GB and Ethereum (Parity) more than 165GB as of this writing.

11] The Merkle-DAGs will be thin in the absence of many concurrent events, or have a high branching factor otherwise. In both cases, branches are consolidated every time a new event is issued from a replica, thus creating thin waists in the DAG.

12] Fast key-value stores, such as in-memory ones, will normally pay a high memory footprint penalty, while disk-backed ones will be slower.
application-specific. We leave the topics of DAG compaction and garbage collection for future work, although we intuitively note that discarding parts of the Merkle-DAG should not be attempted before making sure that every replica is aware of them.

VII. CONCLUSION

In this paper we approached Merkle-DAGs as causality-encoding structures with self-verification and efficient syncing properties. This led us to introduce the concept of Merkle-Clock, demonstrating that they can be described as a state-based CRDT which, announced with a Broadcaster component and fetched with a DAG-Syncer facility, converges in all replicas.

We then presented Merkle-CRDTs as Merkle-Clocks with CRDT payloads. We showed how Merkle-CRDTs work with almost no messaging layer guarantees and no constraints on the replica-set, which can be dynamic and unknown, while providing per-object causal consistency. Merkle-CRDTs are widely used in the IPFS ecosystem for database logging operations\cite{13} in OrbitDB\cite{14}, a distributed, P2P database, its serverless application, Orbit\cite{15}, as well as distributed, collaborative editing\cite{16} and mobile photo-sharing applications\cite{17}.

Merkle-CRDTs are a marriage between traditional blockchains, which need consensus to converge, and CRDTs, which converge by design, and thus inherit positive and negative aspects from both worlds. With this work, we hope to have set a good foundation for further research on the topic.

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