Inclusive $\chi_b J(nP)$ Decays to $D^0 X$

R. A. Briere, T. Ferguson, G. Tatishvili, H. Vogel, M. E. Watkins, J. L. Rosner, J. P. Alexander, D. G. Cassel, J. E. Duboscq, R. Ehrlich, L. Fields, R. S. Galik, L. Gibbons, R. Gray, S. W. Gray, D. L. Hartill, B. K. Heltsley, D. Hertz, J. Kandaswamy, D. L. Kreinick, V. E. Kuznetsov, H. Mahlke-Krüger, D. Mohapatra, P. U. E. Onyisi, J. R. Patterson, D. Peterson, D. Riley, A. Ryd, A. J. Sadoff, X. Shi, S. Stroiney, W. M. Sun, T. Wilksen, S. B. Athar, R. Patel, J. Yelton, P. Rubin, B. I. Eisenstein, I. Karliner, S. Mehrabyan, N. Lowrey, M. Selen, E. J. White, J. Wiss, R. E. Mitchell, D. Besson, T. K. Pedlar, D. Cronin-Hennessy, K. Y. Gao, J. Hietala, Y. Kubota, T. Klein, B. W. Lang, R. Poling, A. W. Scott, P. Zweber, S. Dobbs, Z. Metreveli, K. K. Seth, A. Tomaradze, J. Libby, A. Powell, G. Wilkinson, K. M. Ecklund, W. Love, V. Savinov, A. Lopez, H. Mendez, J. Ramírez, J. Y. Ge, D. H. Miller, I. P. J. Shipsey, B. Xin, G. S. Adams, M. Anderson, J. P. Cummings, I. Danko, D. Hu, B. Moziak, J. Napolitano, Q. He, J. Insler, H. Muramatsu, C. S. Park, E. H. Thorndike, F. Yang, M. Artuso, S. Blusk, S. Khalil, J. Li, R. Mountain, S. Nisar, K. Randrianarivony, N. Sultana, T. Skwarnicki, S. Stone, J. C. Wang, L. M. Zhang, G. Bonvicini, D. Cinabro, M. Dubrovin, A. Lincoln, P. Naik, J. Rademacker, D. M. Asner, K. W. Edwards, and J. Reed

(CLEO Collaboration)
Abstract

Using Υ(2S) and Υ(3S) data collected with the CLEO III detector we have searched for decays of χ_{bJ} to final states with open charm. We fully reconstruct D^0 mesons with p_{D^0} > 2.5 GeV/c in three decay modes (K^−π^+, K^−π^+π^0, and K^−π^−π^+π^+) in coincidence with radiative transition photons that tag the production of one of the χ_{bJ}(nP) states. Significant signals are obtained for the two $J = 1$ states. Recent non-relativistic QCD (NRQCD) calculations of χ_{bJ}(nP) → c ¯cX depend on one non-perturbative parameter per χ_{bJ} triplet. The extrapolation from the observed $D^0X$ rate over a limited momentum range to a full $c ¯cX$ rate also depends on these same parameters. Using our data to fit for these parameters, we extract results which agree well with NRQCD predictions, confirming the expectation that charm production is largest for the $J = 1$ states. In particular, for $J = 1$, our results are consistent with $c ¯c g$ accounting for about one-quarter of all hadronic decays.
I. INTRODUCTION

The six known $\chi^{bJ}(nP)$ $P$-wave bound states of a bottom quark ($b$) and its antiparticle $\bar{b}$ are labeled by their total angular momentum $J = 0, 1, 2$ and radial quantum number $n = 1, 2$. Their decays provide a place to test predictions based on Quantum Chromodynamics (QCD), which describes the strong interaction between quarks in the Standard Model of particle physics. While strong coupling prevents QCD at low energies from being treated with naive perturbation theory, specialized calculational techniques have been developed and applied with general success. In the $b\bar{b}$ system of states, one can study both transitions among the various quantum states, which also include the $S$-wave $\Upsilon$ states, or else study decays which are initiated by annihilation of the quark-antiquark pair. Although the $\chi^{bJ}$ states have been known for many years and there have been several studies of their transitions to other bound states in the $b\bar{b}$ system, there are no published annihilation decay branching fractions. This Article reports the first observation of some of the inclusive decays of the $\chi^{bJ}(1P, 2P)$ to $D^0$ mesons.

In practice, one studies $\chi^{bJ}$ produced via the radiative transitions $\Upsilon(mS) \rightarrow \gamma \chi^{bJ}(nP)$ from $\Upsilon$ mesons produced directly at $e^+e^-$ colliders. The transition photons are typically used to tag $\chi^{bJ}$ events. Most of the $\chi^{bJ}$ radiative decays to the $\Upsilon$ states are well-measured [1]; the largest branching fraction is quite substantial, about 35%. Small, $O(1\%)$, hadronic transitions to other bottomonium states, $\chi_{b1,2}(2P) \rightarrow \pi\pi \chi_{b1,2}(1P)$ and $\chi_{b1}(2P) \rightarrow \omega \Upsilon(1S)$, have recently been observed [2]. The remainder of the decays are expected to be dominated by $b\bar{b}$ annihilation. Positive $C$-parity forbids decays via a single photon; the leading process is annihilation into two gluons. For the $J = 1$ state, decay into two on-shell gluons is forbidden [3]; instead, this state decays preferentially via $q\bar{q}g$. While the $J = 0, 2$ decay widths are dominated by this $gg$ process, they also have a small admixture of $q\bar{q}g$.

We observe $b\bar{b}$ annihilation as a decay into lighter hadrons and are seeking to determine whether production of charm hadrons is suppressed or not. It is well-known that in continuum $e^+e^-$ production ($e^+e^- \rightarrow \gamma \rightarrow q\bar{q}$) that charm is not suppressed, while in $ggg$ decays of the $\Upsilon(1S)$, an upper limit on $D^{*+}$ production of $\mathcal{B}(\Upsilon(1S) \rightarrow ggg \rightarrow D^{*+}X) < 1.9\%$ (90\% CL) indicates significant suppression [4].

The earliest calculations of inclusive charm ($ccX$) production from bottomonia focused on $\Upsilon \rightarrow ggg$ decays, giving estimates of a few percent [5]. It was soon pointed out that while production of $ccX$ is predicted to be suppressed in $gg$ hadronization, it is not expected to be suppressed in $q\bar{q}g$ hadronization [6]. Since the $gg$ process is absent for the $\chi_{b1}(nP)$ states, they should have higher branching fractions to $ccX$. These first calculations exhibited infrared divergences manifested as logarithms of the binding energy which were estimated in terms of a confinement radius. The predicted ratios of branching fractions are [6] $R^{(c)}_{ij} \equiv \mathcal{B}(\chi_{bJ} \rightarrow gg, q\bar{q}g \rightarrow ccX)/\mathcal{B}(\chi_{bJ} \rightarrow gg, q\bar{q}g) = 6\%, 25\%,$ and 12\% for the $J = 0, 1,$ and 2 states, respectively. The predictions were independent of the radial quantum number, $n$. The 25\% branching fraction for $J = 1$ corresponds to equal rates for all accessible quark flavors $q$ in $q\bar{q}g$.

With the development of non-relativistic QCD (NRQCD) techniques [7], a proper treatment of the infrared divergences was given and thus much improved calculations became possible. However, initial work [8] on bottomonium decays approximated final-state quarks as massless. Recently, this was remedied, and detailed NRQCD calculations of massive charm production in $\chi_{bJ}$ decay have been performed [9]. Decay rates are expressed in terms of one non-perturbative parameter per $\chi_{bJ}$ triplet: $\rho_8 \equiv m^2_8 \langle \mathcal{O}_8 \rangle/\langle \mathcal{O}_1 \rangle$ where $\mathcal{O}_1$ ($\mathcal{O}_8$) is a...
particular color-singlet (color-octet) four-quark operator \[8, 9\] and \(m_b\) is the one-loop pole mass, \(m_b \simeq 4.6\text{ GeV}/c^2\). All of the \(n\)-dependence in these calculations is contained in \(\rho_8\), and \(R_J^{(c)}\) is found to increase monotonically with increasing \(\rho_8\). For illustrative purposes, we choose a common nominal value of \(\rho_8 = 0.10\), which gives \(R_J^{(c)} = 5\%, 23\%,\) and \(8\%\) for the \(J = 0, 1,\) and 2 states, respectively. These results are in general agreement with the older calculation cited above. In particular, charm production is expected to be largest for the \(J = 1\) states. Not only the predicted \(R_J^{(c)}\), but also the efficiency of our applied \(D^0\) momentum cut, depend on \(\rho_8\). We thus fit for \(\rho_8\) in the context of the NRQCD results in order to interpret the consistency of our results with theory.

To summarize, we observe charm production by observing \(D^0\) mesons in \(\chi_bJ\) decays. We thereby hope to test predictions for the branching fractions, especially the expectation that the largest branching fractions will come from the \(J = 1\) states due to the dominance of \(q\overline{q}g\) decays when \(gg\) is absent. Sections II-VII present our experimental results for inclusive decays of \(\chi_bJ\) to \(D^0X\), with a \(D^0\) momentum cut. Section VIII makes the connection between these measurements and the theoretically-predicted total rate of \(c\overline{c}X\) production, \(R_J^{(c)}\). Section IX summarizes our conclusions.

II. THE CLEO III EXPERIMENT AND DATA SETS

We use data collected with the CLEO III detector \[10\] at the Cornell Electron Storage Ring (CESR). Charged particle tracking is provided by a four-layer silicon tracker and a 47-layer drift chamber \[11\] covering 93\% of the solid angle. Particle identification (PID) is performed via specific ionization measurements \((dE/dx)\) in the drift chamber supplemented by a Ring-Imaging Cherenkov detector (RICH) \[12\] which covers 80\% of the solid angle. Photons are detected using an electromagnetic calorimeter consisting of 7784 CsI(Tl) crystals \[13\]. All of these detector elements are immersed in a 1.5 T solenoidal magnetic field.

We use CLEO III data samples of 0.65, 1.27, and 1.40 \(\text{fb}^{-1}\) at the \(\Upsilon(1S), \Upsilon(2S),\) and \(\Upsilon(3S)\) resonances, corresponding to 13.0, 9.4, and 6.1 million \(\Upsilon\) mesons produced, respectively. In addition, data were also collected about 25 MeV below each resonance: we analyze 0.14, 0.43, and 0.16 \(\text{fb}^{-1}\) from below the \(\Upsilon(1S), \Upsilon(2S),\) and \(\Upsilon(3S)\) resonances, respectively. We do not use a direct off-resonance subtraction, but rather use these samples to constrain background shapes.

III. EXPERIMENTAL TECHNIQUE

This analysis includes all six known \(\chi_{bJ}(nP)\) states: \(J = 0, 1,\) and 2 and \(n = 1\) and 2. The \(\chi_{bJ}\) states produced in radiative \(\Upsilon\) decays are tagged by transition photons from \(\Upsilon \to \gamma \chi_{bJ}\) decays; the \(\chi_{bJ}\) yields are obtained from fits to \(E_\gamma\) spectra. We then fit \(E_\gamma\) spectra from events with a \(D^0\) candidate in the signal mass region, using \(D^0\) mass sidebands to remove combinatorial background under the \(D^0\) signal peak. After correcting for \(D^0\) efficiencies and branching fractions, the ratio of these two inclusive yields determines the fraction of \(\chi_{bJ}\) decays with a true \(D^0\) (above our \(D^0\) minimum momentum requirement). The photon efficiencies, numbers of initial \(\Upsilon(nS)\), and many associated systematic uncertainties largely cancel.

We finally apply some small corrections to obtain the rate for direct production of \(D^0\) mesons in \(\chi_{bJ}\) decays. Direct denotes the exclusion of charm production in decays of other
bottomonium states produced by transitions from our initial $\chi_{bJ}$ (for example, via $\gamma, \pi\pi, \omega$ transitions). Our focus is on direct $D^0$ production via hadronization of $\chi_{bJ} \rightarrow qg, q\bar{q}g$ decays only, and not on transitions to other $b\bar{b}$ states which subsequently decay to $D^0X$.

IV. EVENT SELECTION

We first select events with transition photon candidates with energies between $3.50 < \ln(E_\gamma \text{[MeV]}) < 5.70$ ($33 < E_\gamma < 299$ MeV). Only showers in the barrel calorimeter, $|\cos \theta| < 0.8$, that are isolated from charged tracks are considered. Hadronic shower fragments are suppressed by vetoing any candidate photon shower that has a charged track pointing anywhere in the candidate’s “connected region”: this is a contiguous group of adjacent crystals with the energy deposition in each crystal, $E_{\text{xtal}}$, satisfying $E_{\text{xtal}} > 10$ MeV. An additional requirement on the fraction of energy deposited in the central $3 \times 3$ square of a $5 \times 5$ square, $E9/E25$, is applied. We use an energy-dependent $E9/E25$ criterion to select soft transition photon candidates, while photons later used in forming $\pi^0$ candidates, both as a veto and as $D^0$ decay daughters, must satisfy the requirement of $E9/E25 > 0.85$.

Photon background in the $\Upsilon \rightarrow \gamma \chi_{bJ}$ transitions is dominated by $\pi^0$ decay products. To suppress this background, we reject photon candidates that, when combined with any other photon, form a $\pi^0$ candidate that has an invariant mass within three standard deviations of the nominal $\pi^0$ mass and a lab-frame opening angle between the two photons satisfying $|\cos \theta_{\gamma\gamma}| > 0.7$.

For $D^0$ reconstruction, we select well-measured tracks consistent with originating from the interaction point. These tracks must have an impact parameter of less than 5 cm with respect to the interaction point along the beam direction, and less than 5 mm with respect to it in the transverse plane. Charge-conjugate final states, $D^0X$, are also included and are implied in the remainder of the paper. Candidate $D^0$ mesons are reconstructed via three decay modes: $K^{-}\pi^+, K^{-}\pi^+\pi^0$, and $K^{-}\pi^-\pi^+\pi^+$. For charged pion and kaon selection, particle identification combines RICH measurements with $dE/dx$ in a momentum-dependent manner. The $dE/dx$ information is expressed as $\sigma_{\pi,K}^{dE}$, the number of standard deviations between measured and expected ionization for the $\pi, K$ hypothesis. The track-dependent $dE/dx$ resolution used to normalize $\sigma_{\pi,K}$ includes dependencies on velocity, $\cos \theta$, and the number of hits used for $dE/dx$. RICH information is characterized with a likelihood $L$; we use $L_{\pi,K}$ as shorthand for $-2 \ln L_{\pi,K}$. When used, the RICH information is combined with $dE/dx$ into one combined separation variable as: $\Delta x_{\pi,K}^2 = L_{\pi,K} - L_{K,\pi} + (\sigma_{\pi,K}^{dE})^2 - (\sigma_{K,\pi}^{dE})^2$. The first (second) subscript is chosen for $\pi$ ($K$) identification. We also impose requirements on the number of detected Cherenkov photons, $n_{\gamma}^{\pi,K}$, for either the $\pi$ or $K$ hypothesis in the RICH detector.

Momentum dependence in the use of the RICH is motivated by the Cherenkov threshold for kaons and the need for tracks to have sufficient transverse momentum to reach the RICH detector given their curvature in the magnetic field. All pion candidates must satisfy $|\sigma_{\pi}^{dE}| < 3$. Pion candidates with $p < 0.50$ GeV/c are accepted with that criteria alone, but additional requirements are added for some higher-momentum candidates. If $0.50 < p < 0.65$ GeV/c and $n_{\gamma}^{\pi} > 2$, we also require $\Delta x_{\pi}^2 < 0$. Candidates with $p > 0.65$ GeV/c must satisfy both $n_{\gamma}^{\pi} > 2$ and $\Delta x_{\pi}^2 < 0$.

Kaons are identified in an analogous manner to pions, with three additional criteria. First, kaon candidates must satisfy $p > 0.18$ GeV/c. Kaons lose more energy in the inner detector than pions, and tightly curling tracks are poorly reconstructed. Second, if the
track momentum is greater than 0.60 GeV/c, then the track must also be within the RICH fiducial region, |cos θ| < 0.80; this ensures good rejection of the more numerous pions as the dE/dx separation degrades. Finally, when RICH information is available, a tighter criterion, ∆χ² < 10, is used compared to that employed for pions due to the relative abundance of pions over kaons.

The π⁰ meson candidates from D⁰ → K⁻π⁺π⁰ are reconstructed from pairs of photons with an invariant mass within 2.5 standard deviations of the nominal π⁰ mass. These candidates are then kinematically constrained to the π⁰ mass. For the K⁻π⁺π⁰ mode, the precision is improved with an additional requirement on the candidate’s location in the Dalitz plot. Our criteria retains the 70% of decays from the most densely-populated regions of phase space (based on previous measurements [14]).

In order to avoid the large combinatorial backgrounds under the D⁰ signal at lower momenta, only candidate D⁰ momenta p_D⁰ > 2.5 GeV/c are accepted. Figure 1 shows the sum of the K⁻π⁺, K⁻π⁺π⁰, and K⁻π⁻π⁺π⁺ invariant mass distributions, Knπ (n = 1, 2, 3), obtained from Υ(2S) and Υ(3S) data for events also containing transition photon candidates. The D⁰ signal region is defined as the K⁻π⁺, K⁻π⁺π⁰, and K⁻π⁻π⁺π⁺ invariant mass interval ±2.5σ_m (using a mode-averaged σ_m ≃ 0.0075 GeV/c²) from the nominal D⁰ mass, m_D⁰ [1]. The D⁰ “sideband” regions, each with a width of 2.5σ_m, are located symmetrically, between 7.5 σ_m and 10.0 σ_m on either side of the nominal D⁰ mass.

V. FITS TO THE PHOTON ENERGY SPECTRA

We first measure the total number of χ_bJ tagged with an observed transition photon by fitting the inclusive E_γ spectrum. Photon peaks from inclusive Υ(2S) → γχ_bJ(1P) and Υ(3S) → γχ_bJ(2P) transitions are evident in Fig. 2.
We use $\Upsilon(1S)$ resonance and $\Upsilon(nS)$ off-resonance data to model the photon background in the $E_\gamma$ spectra [15]. The off-resonance data are observed to have indistinguishable spectra in our energy region and thus the three samples are combined to increase statistics. The $\Upsilon(1S)$ on-resonance and $\Upsilon(nS)$ off-resonance shapes are also quite similar, and we initially fit with two independent normalizations to peak-free regions of the photon energy spectrum. The regions are defined by $3.50 < \ln(E_\gamma [\text{MeV}]) < 3.70$ ($33 \text{ MeV} < E_\gamma < 40 \text{ MeV}$) and $5.55 < \ln(E_\gamma [\text{MeV}]) < 5.70$ ($257 \text{ MeV} < E_\gamma < 299 \text{ MeV}$) and the fit results are used to then fix the relative normalization of these on- and off-resonance samples for subsequent signal fits.

When fitting the full photon energy spectra to extract signal yields, only one overall normalization parameter for the background is varied. We find, however, that the fit quality is acceptable only after the inclusion of first- ($1P$) or second-order ($2P$) polynomials to allow small smooth adjustments of the background shape. The fit also includes signal contributions from the three dominant $E1$ transitions, $\Upsilon(2S) \rightarrow \gamma\chi_{bJ}(1P)$ or $\Upsilon(3S) \rightarrow \gamma\chi_{bJ}(2P)$, as appropriate. The $\chi_{bJ}(1P)$ and $\chi_{bJ}(2P)$ signal peaks are described by a so-called Crystal Ball line shape [16] with fixed asymmetry parameters, $\alpha$ and $n$. This line shape is a Gaussian, described by a peak energy $E_p$ and resolution $\sigma_E$, matched with the constant $c$ onto an asymmetric low energy tail, $1/(E_p - E + c)^n$, at an energy $E_p - \alpha \sigma_E$. We obtain $E_p$ from published results [1] and use the values $\alpha = 0.84$ and $n = 25.8$. The values of $\sigma_E/E$ depend on $E$, varying from 5.4% to 3.9% as the energy of the six transition lines increases. This $E$ dependence is determined from Monte-Carlo studies, but the overall scale of the resolution is adjusted based on fits to data. In addition to the dominant $\Upsilon(3S) \rightarrow \gamma\chi_{bJ}(2P)$ transitions, the fit to the $\Upsilon(3S)$ spectrum includes the lines due to $\chi_{bJ}(2P) \rightarrow \gamma\Upsilon(2S)$ cascades. The fit results are displayed with the data in Fig. 2 and tabulated in Tables I and II.

Photon energy spectra for events with $D^0$ mesons are obtained by subtracting the $\ln(E_\gamma [\text{MeV}])$ spectra associated with the $K\pi n\pi$ ($n = 1, 2, 3$) $D^0$ sidebands from the $D^0$ signal region. The $\ln(E_\gamma [\text{MeV}])$ distributions and the fits for the $\Upsilon(2S)$ and $\Upsilon(3S)$ data are
FIG. 3: Fits to the $\Upsilon(2S)$ (left) and $\Upsilon(3S)$ (right) photon energy spectrum obtained for events with $D^0$ mesons. The data are shown as dots; the fits are shown as histograms; the dashed lines represents the total fitted background.

FIG. 4: Energy spectrum for background-subtracted $\Upsilon(2S) \to \gamma \chi_{bJ}(1P)$ (left) and $\Upsilon(3S) \to \gamma \chi_{bJ}(2P)$ (left) photon lines obtained for events with $D^0$ mesons. The data are shown as dots; the fit is shown as the solid line. Individual contributions from the signal $\Upsilon(mS) \to \gamma \chi_{bJ}(nP)$ lines are shown as dashed-line peaks.

presented in Fig. 3. The $J = 1$ lines are the most pronounced. Photon background shapes for these spectra are the same as for the $\Upsilon(2S)$ and $\Upsilon(3S)$ inclusive photon analysis, except that an acceptable fit quality is obtained without the addition of low-order polynomials, and they are omitted. The background-subtracted photon spectra are presented in Fig. 4 and fit results are tabulated in Tables I and II.

VI. MEASUREMENT OF $\chi_{bJ} \to D^0X$ ($p_{D^0} > 2.5$ GeV/c) RATES

The yields of events with $\chi_{bJ}$ and $D^0$ mesons ($D^0 \to K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^-\pi^+\pi^+$) include non-direct $\chi_{bJ}$ decays which must be subtracted. Non-direct $\chi_{bJ}(1P)$ decays to $D^0X$
include $\Upsilon(2S) \rightarrow \gamma \chi_{bJ}(1P)$; $\chi_{bJ}(1P) \rightarrow \gamma \Upsilon(1S)$ decays where $D^0$ mesons are then produced in $\Upsilon(1S)$ annihilation into $ggg, gg\gamma$, and $\gamma$.

Non-direct $\chi_{bJ}(2P)$ decays to $D^0X$ similarly include production of bottomonium states which in turn may decay to $D^0X$. Known processes include $\Upsilon(1S)$ produced via $\Upsilon(3S) \rightarrow \gamma \chi_{bJ}(2P)$ followed by

- $\chi_{bJ}(2P) \rightarrow (\gamma, \omega) \Upsilon(1S)$
- $\chi_{bJ}(2P) \rightarrow \gamma \Upsilon(2S); \Upsilon(2S) \rightarrow (\pi\pi, \pi^0, \eta) \Upsilon(1S)$
- $\chi_{bJ}(2P) \rightarrow \pi\pi\chi_{bJ}(1P); \chi_{bJ}(1P) \rightarrow \gamma \Upsilon(1S)$

and $\chi_{bJ}(1P)$ produced via $\Upsilon(3S) \rightarrow \gamma \chi_{bJ}(2P)$ followed by

- $\chi_{bJ}(2P) \rightarrow \pi\pi\chi_{bJ}(1P)$
- $\chi_{bJ}(2P) \rightarrow \gamma \Upsilon(2S); \Upsilon(2S) \rightarrow \gamma \chi_{bJ}(1P)$

and $\Upsilon(2S)$ from $\Upsilon(3S) \rightarrow \gamma \chi_{bJ}(2P); \chi_{bJ}(2P) \rightarrow \gamma \Upsilon(2S)$.

Yields for events with $D^0$ mesons from direct $\chi_{bJ}(1P)$ decays are calculated by correcting raw yields from the $\Upsilon(2S)$ data with a non-direct rate determined using known branching fractions [1] and an $\Upsilon(1S) \rightarrow (ggg, gg\gamma, \gamma) \rightarrow D^0X$ rate for $p_{D^0} > 2.5$ GeV/c of $2.60 \pm 0.50\%$ [17]. We estimate the numbers of these non-direct events as $16 \pm 9, 191 \pm 58, and 125 \pm 34$ for $J = 0, 1$, and 2, respectively. Corresponding estimates of the non-direct backgrounds for $\chi_{bJ}(2P) \rightarrow D^0X$ in the $\Upsilon(3S)$ data are $53 \pm 24, 392 \pm 70, and 311 \pm 50$ for $J = 0, 1$, and 2, respectively. We account for the fact that prompt production of $D^0X$ from $\Upsilon(2S)$ differs from that from $\Upsilon(1S)$ due to the different mixture of decays mediated by $ggg, gg\gamma$, and $\gamma$.

Yields for inclusive $\chi_{bJ}$ production, total $\chi_{bJ}$ with $D^0$ mesons, and $\chi_{bJ}$ with directly-produced $D^0$ mesons, are summarized in Tables I and II. In addition, we list a correction due to a small observed curvature in the $Kn\pi$ mass spectra leading to a small residual background of true photons and fake $D^0$ mesons, since our sideband subtraction assumes a flat background.

The direct $\chi_{bJ}$ yields, $N_{\chi_{bJ}}^{D^0,\text{dir}}$, from $N_{\Upsilon}$ initial $\Upsilon$ produced are:

$$N_{\chi_{bJ}}^{D^0,\text{dir}} = N_{\Upsilon} \epsilon_{\gamma} B(\Upsilon \rightarrow \gamma \chi_{bJ}) B(\chi_{bJ} \rightarrow gg, q\bar{q}g \rightarrow D^0X) \sum \epsilon_i B_i(D^0),$$

where $\epsilon_{\gamma}$ is the $\gamma$ detection efficiency and the last factor $\sum \epsilon_i B_i(D^0)$ is a sum over the three $Kn\pi$ decay modes of the $D^0$. The observed number of inclusive $\chi_{bJ}$ decays is given by

$$N_{\chi_{bJ}}^{\text{Incl}} = N_{\Upsilon} \epsilon_{\gamma} B(\Upsilon \rightarrow \gamma \chi_{bJ}).$$

Our main results, the branching fractions $B(\chi_{bJ} \rightarrow gg, q\bar{q}g \rightarrow D^0X)$, are obtained from the two previous equations as:

$$B(\chi_{bJ} \rightarrow gg, q\bar{q}g \rightarrow D^0X) = \frac{N_{\chi_{bJ}}^{D^0}}{N_{\chi_{bJ}}^{\text{Incl}} \sum \epsilon_i B_i(D^0)},$$

where the photon efficiency, $\epsilon_{\gamma}$, and sample size, $N_{\Upsilon}$, both cancel. For determination of the $D^0$ detection efficiencies, Monte-Carlo simulation of continuum $c\bar{c}$ events (based on Jetset
were used, since this sample is expected to approximate the jet-like events from the \( \chi_{bJ} \rightarrow c \bar{c} q \bar{q} \) decays. We find that the efficiency is consistent with being independent of momentum in the \( p_{D^0} > 2.5 \text{ GeV}/c \) range.

Based on detailed comparisons of particle identification in our data and Monte-Carlo simulations, we conclude that small efficiency corrections are needed. The \( Kn\pi \) modes receive adjustments of \( f_Kf_\pi \), where \( f_K = 0.95(0.99) \) and \( f_\pi = 0.99(1.01) \) for \( \Upsilon(2S) \) (\( \Upsilon(3S) \)) data. The \( \chi_{bJ} \rightarrow D^0X \) decay rates for \( p_{D^0} > 2.5 \text{ GeV}/c \) are presented in Tables I and II.

### TABLE I: \( \Upsilon(2S) \rightarrow \gamma\chi_{bJ}(1P) \) (\( J = 0, 1, 2 \)) transition yields and \( \chi_b \rightarrow gg, q\bar{q}g \rightarrow D^0X \) rates, for \( p_{D^0} > 2.5 \text{ GeV}/c \). Errors shown are statistical only.

| Final state            | \( \chi_{b0}(1P) \) | \( \chi_{b1}(1P) \) | \( \chi_{b2}(1P) \) |
|------------------------|-----------------------|-----------------------|-----------------------|
| \( N_{\chi_{bJ}}^{\text{Incl}} \) | 166860 ± 5988 | 363825 ± 6793 | 379457 ± 7243 |
| \( N_{\chi_{bJ}}^{D^0} \) (raw) | 501 ± 303 | 2561 ± 346 | 1207 ± 360 |
| \( D^0 \) sideband correction | 11 ± 5 | 60 ± 6 | 57 ± 7 |
| non-direct \( D^0 \) | 16 ± 9 | 191 ± 58 | 125 ± 34 |
| \( N_{\chi_{bJ}}^{D^0,\text{dir}} \) (direct) | 474 ± 303 | 2310 ± 351 | 1025 ± 362 |
| \( B(\chi_{bJ}(1P) \rightarrow gg, q\bar{q}g \rightarrow D^0X) \) | 5.63 ± 3.61% | 12.59 ± 1.94% | 5.36 ± 1.90% |

### TABLE II: \( \Upsilon(3S) \rightarrow \gamma\chi_{bJ}(2P) \) (\( J = 0, 1, 2 \)) transition yields and \( \chi_b \rightarrow gg, q\bar{q}g \rightarrow D^0X \) rates, for \( p_{D^0} > 2.5 \text{ GeV}/c \). Errors shown are statistical only.

| Final state            | \( \chi_{b0}(2P) \) | \( \chi_{b1}(2P) \) | \( \chi_{b2}(2P) \) |
|------------------------|-----------------------|-----------------------|-----------------------|
| \( N_{\chi_{bJ}}^{\text{Incl}} \) | 219773 ± 5201 | 491818 ± 5197 | 524549 ± 5628 |
| \( N_{\chi_{bJ}}^{D^0} \) (raw) | 565 ± 341 | 2757 ± 366 | 477 ± 370 |
| \( D^0 \) sideband correction | 39 ± 7 | 122 ± 7 | 122 ± 7 |
| non-direct \( D^0 \) | 53 ± 24 | 392 ± 70 | 311 ± 50 |
| \( N_{\chi_{bJ}}^{D^0,\text{dir}} \) (direct) | 473 ± 342 | 2243 ± 373 | 44 ± 373 |
| \( B(\chi_{bJ}(2P) \rightarrow gg, q\bar{q}g \rightarrow D^0X) \) | 4.13 ± 3.00% | 8.75 ± 1.47% | 0.16 ± 1.37% |

### VII. SYSTEMATIC UNCERTAINTIES ON THE BRANCHING FRACTIONS

Systematic uncertainties on the six measured branching fractions are primarily of two types. The first are uncertainties in \( D^0 \) reconstruction; these affect each of the six \( \chi_{bJ} \) states equally and are summarized in Table III. The next are uncertainties related to our photon yields, both in terms of efficiencies and yield extractions. These often differ for the six \( \chi_{bJ} \) states, and are summarized in Table IV. In the remainder of this section we detail the sources of the uncertainty estimates presented in the aforementioned Tables.
The first three entries of Table III involve efficiencies for track-finding, $\pi^0$ reconstruction, and particle identification algorithms. Since the composition of the three $D^0$ final states differ, we take a linear weighting of the uncertainties across $D^0$ modes. The weights used are $w_i = \epsilon_i B_i / \sum_j \epsilon_j B_j$, yielding 0.25, 0.34, and 0.41 for $D^0 \to K^- \pi^+$, $D^0 \to K^- \pi^+ \pi^0$, and $D^0 \to K^- \pi^+ \pi^+$, respectively.

The systematic uncertainty in track-finding is obtained by studies of the difference between data and Monte-Carlo simulation. We assign a 1.5% uncertainty per track, which gives a net uncertainty of 4.2% after weighting across $D^0$ decay modes.

We assess the uncertainty in $\pi^0$-finding at 5% per $\pi^0$. Taking into account the weight of the $D^0 \to K^- \pi^- \pi^0$ mode, the net $\pi^0$-finding systematic uncertainty is 1.7%.

Systematic uncertainties in kaon and pion identification are obtained by comparing data and Monte-Carlo efficiencies. We obtain 2% (1%) uncertainties per $K$ ($\pi$) which yield a net 4.0% systematic uncertainty, averaged over $D^0$ modes.

The systematic uncertainty on the $D^0 \to K^- \pi^+ \pi^0$ efficiency due to selection on the Dalitz region is obtained by comparing the inclusive yield changes in data compared to Monte-Carlo simulations as the selection efficiency is varied. As a result of this study, and accounting for the fraction of $D^0$ candidates found via this decay mode, we assign 1.0% as our total Dalitz region selection uncertainty.

For evaluation of systematic uncertainties related to the $D^0$ momentum requirement, the $p_{D^0}$ requirement was varied. Events were selected for three values of the $D^0$ momentum requirement ($> 2.2$, $> 2.5$, and $> 2.8$ GeV/c). We assign a 1.7% branching fraction uncertainty due to this source.

To study possible effects of the event shape and environment on the $D^0$ detection efficiency, different models of signal Monte-Carlo and continuum Monte-Carlo events are analyzed. Results indicate a 3.0% uncertainty of the efficiency for the event-shape changes explored.

Systematic uncertainties related to the definition of the $D^0$ signal and sideband regions are obtained by varying the corresponding mass windows. This also includes uncertainty due to a nonlinear background shape under the $D^0$ signal. The total systematic uncertainty is determined to be 2.5%.

The total uncertainty in the $D^0$ efficiency is 7.5% for each $\chi_{bJ}$ state, as noted in Table III. We now turn to the photon-related systematic uncertainties presented in Table IV.

**TABLE III:** Relative systematic uncertainties on measured branching fractions from sources affecting the $D^0$ efficiency.

| Source                                              | Uncertainty (%) |
|-----------------------------------------------------|-----------------|
| Tracking: 1.5%/track                                | 4.2             |
| $\pi^0$ efficiency: 5%/\$\pi^0$                     | 1.7             |
| PID: 2%/K\pm, 1%/\$\pi^\pm$                         | 4.0             |
| $K\pi\pi^0$ Dalitz requirement                      | 1.0             |
| Momentum dependence                                 | 1.7             |
| Decay model effects on $D^0$ efficiency              | 3.0             |
| Selection of events with a $D^0$                    | 2.5             |
| Total $D^0$-related systematic uncertainty          | 7.5             |
To verify that the photon efficiency largely cancels in our analysis, the difference of photon efficiencies between inclusive events and those with a $D^0$ candidate is studied using Monte-Carlo samples. We find that the relative photon efficiency difference between spherical $ggg$ events and jet-like $q\bar{q}$ events is about 6%. In our case, we are concerned about the difference between generic $\chi_{bJ}$ events and those having a reconstructed $D^0$. Presumably the effect of this bias is smaller than that of the rather large overall event shape change between these two Monte-Carlo samples. We thus take $1/3$ of the variation and assign a 2% uncertainty for all six $\chi_{bJ}$ states.

For estimation of line-shape fitting uncertainties we change the Crystal Ball line-shape parameters $\alpha$ and $n$ by $\pm 10\%$ from their nominal values. This range is chosen as appropriate based on changes in fit quality. We take the resulting branching fraction variations as systematic uncertainties, ranging from 0.1% to 0.6%.

The nominal fitting ranges for photon energy distributions are $3.8 < \ln(E_\gamma [\text{MeV}]) < 5.5$ for $\Upsilon(2S)$ and $3.8 < \ln(E_\gamma [\text{MeV}]) < 5.7$ for $\Upsilon(3S)$. We vary the lower and upper limits of the fitting regions from 3.50 to 3.70 and from 5.50 to 5.70. Variations in our results suggest uncertainties from 0.3% to 0.6%.

As mentioned above, the photon background shape consists of two components: the resonant and off-resonance photon spectra used to estimate the background shapes in the $\Upsilon(2S)$ and $\Upsilon(3S)$ photon energy distributions. We varied scaling factors for the photon background components and changed the $\Upsilon(1S)$ resonance and the $\Upsilon(2S)$, $\Upsilon(3S)$ off-resonance contributions in the photon background shape. Also, in the fit of the $\Upsilon(2S)$ and $\Upsilon(3S)$ inclusive photon energy distributions, we used additional background components to obtain a better fit quality. First, second, and third order polynomials are tried as extra components in addition to the $\Upsilon(1S)$ on-resonance and the $\Upsilon(2S)$ and $\Upsilon(3S)$ off-resonance background shapes. We estimate systematic uncertainties due to such choices at levels ranging from 0.5% to 1.6%.

Our nominal fit uses logarithmic binning of energy $\ln(E_\gamma [\text{MeV}])$. We changed the logarithmic energy scale to linear binning, with 1 MeV energy bins. The photon background shape was left unchanged. We assign from 0.2% to 1.7% uncertainties on our branching fractions based on the stability of our results.

The $\Upsilon(3S)$ photon energy spectrum includes $\Upsilon(2S) \rightarrow \gamma \chi_{bJ}(1P)$ transition lines at similar energies. To estimate systematic uncertainties on the $B(\chi_{bJ}(2P) \rightarrow D^0 X)$, we include these lines in the fit to the $\Upsilon(3S)$ inclusive photon spectrum and the photon spectrum for events with $D^0$ mesons. Estimated systematic uncertainties varied from 0.2% to 1.5%.

In Table IV, we summarize the systematic uncertainties associated with $\gamma$ detection and fitting for each of the six $\chi_{bJ}$ lines. Note that these uncertainties apply to the raw yields, before any subtractions are made.

We also performed several simple cross-checks to investigate the stability and consistency of our results. These included splitting the datasets into two subsets, varying selection criteria, and comparing yields in individual $D^0$ decay modes. All of these tests produced consistent results.

Our final results for $p_{D^0} > 2.5$ GeV/$c$ are given in Table V. Upper limits are given for modes without significant signals, but central values for those modes will be needed for fits later.
TABLE IV: Relative systematic uncertainties on measured branching fractions due to sources related to the $E_\gamma$ distributions.

| Source                        | $\chi_{b0}(1P)$ | $\chi_{b1}(1P)$ | $\chi_{b2}(1P)$ | $\chi_{b0}(2P)$ | $\chi_{b1}(2P)$ | $\chi_{b2}(2P)$ |
|-------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $\gamma$ efficiency cancellation | 2.0             | 2.0             | 2.0             | 2.0             | 2.0             | 2.0             |
| Line-shape fitting            | 0.6             | 0.1             | 0.4             | 0.5             | 0.1             | 0.5             |
| Fitting range                 | 0.5             | 0.3             | 0.4             | 0.6             | 0.3             | 0.5             |
| Background shape              | 1.4             | 0.6             | 0.9             | 1.6             | 0.5             | 0.9             |
| $\gamma$ energy binning       | 1.4             | 0.2             | 0.5             | 1.7             | 0.3             | 0.6             |
| $\Upsilon(2S) \rightarrow \gamma \chi_{bJ}(1P)$ lines | –               | –               | –               | 1.5             | 0.3             | 0.2             |
| Total $\gamma$ systematic uncertainty | 2.9             | 2.1             | 2.3             | 3.5             | 2.1             | 2.4             |

TABLE V: Summary of measured branching fractions (or upper limits) for $\mathcal{B}(\chi_{bJ}(nP) \rightarrow gg, q\bar{q}g \rightarrow D^0X)$ with the requirement that $p_{T,D^0} > 2.5$ GeV/c. The uncertainties are statistical and systematic, respectively.

| State | $\mathcal{B}(\chi_{bJ}(nP) \rightarrow gg, q\bar{q}g \rightarrow D^0X)$ (%) | 90% CL | UL (%) |
|-------|--------------------------------------------------------------------------|--------|--------|
| $\chi_{b0}(1P)$ | 5.6 $\pm$ 3.6 $\pm$ 0.5                                                 | < 10.4 |
| $\chi_{b1}(1P)$ | 12.6 $\pm$ 1.9 $\pm$ 1.1                                                |        |
| $\chi_{b2}(1P)$ | 5.4 $\pm$ 1.9 $\pm$ 0.5                                                 | < 7.9  |
| $\chi_{b0}(2P)$ | 4.1 $\pm$ 3.0 $\pm$ 0.4                                                 | < 8.2  |
| $\chi_{b1}(2P)$ | 8.8 $\pm$ 1.5 $\pm$ 0.8                                                 |        |
| $\chi_{b2}(2P)$ | 0.2 $\pm$ 1.4 $\pm$ 0.1                                                 | < 2.4  |

VIII. INTERPRETATION

We observe significant production of $D^0$ mesons from both the $\chi_{b1}(1P)$ and $\chi_{b1}(2P)$ states. There is evidence of a signal for $\chi_{b2}(1P)$, while data for the other three states are inconclusive. For each triplet, we observe the largest branching fraction for the $J = 1$ states, as expected.

The NRQCD calculation mentioned earlier [9] makes predictions for the total $c\bar{c}X$ production rate, $R_j^{(c)}$, as a function of one non-perturbative parameter, $\rho_8$, per $\chi_{bJ}$ triplet. We would like to convert our measurement of the inclusive $D^0X$ rate, with a minimum momentum requirement, into an experimental value for $R_j^{(c)}$. However, this conversion also depends on $\rho_8$, since this parameter affects the momentum spectrum of the $D^0$ mesons and hence the efficiency of our minimum momentum requirement. We use six branching fraction results to determine two best-fit values of $\rho_8$ (one per triplet). Our experimental results for $R_j^{(c)}$ are based on these best-fit values and clearly depend on our use of the NRQCD calculation.

We first discuss the details of how to relate our measurements to the inclusive $c\bar{c}X$ rate.
and then present our extraction of the $\rho_8$ parameter and experimental values of $R_j^{(c)}$. Three factors will combine to cause our extracted $R_j^{(c)}$ to be larger than the directly-measured branching fractions in Table V. We only see some of the $D^0$ spectrum, not all charm appears as $D^0$, and $R_j^{(c)}$ is normalized to the number of $\chi_{bJ}$ that decay via annihilation, not the total number produced. Only one factor works in the other direction: $R_j^{(c)}$ measures $c\bar{c}X$ production, and either charm quark may form a $D^0$.

Suppressing the $\chi_{bJ}(nP)$ radial quantum numbers for simplicity, we have:

$$ R_j^{(c)} = \frac{\mathcal{B}(\chi_{bJ} \to gg, q\bar{q}g \to c\bar{c}X)}{\mathcal{B}(\chi_{bJ} \to gg, q\bar{q}g)} = \frac{\mathcal{B}(\chi_{bJ} \to gg, q\bar{q}g \to D^0X, p_{D^0} > 2.5 \text{ GeV}/c)}{f_{D^0} f_{D^0} \mathcal{B}(\chi_{bJ} \to gg, q\bar{q}g)}, $$

where the right-hand side contains our directly-measured branching fraction with three additional factors which we now explain.

First, we must divide by $\mathcal{B}(\chi \to gg, q\bar{q}g)$ such that the final branching fraction is normalized to only $gg, q\bar{q}g$ decays of the $\chi_{bJ}$ since this is the normalization used for the theoretical prediction. These branching fractions are calculated as $1 - \sum_i B_i$, where the sum extends over all known transitions of a given $\chi_{bJ}$ to other bottomonium states [1].

Next, we divide by $f_2.5$, the fraction of the $D^0$ spectrum expected to be above our $2.5 \text{ GeV}/c D^0$ momentum requirement. This is obtained from the results of Ref. [9], and it depends on the value of $\rho_8$ and knowledge of the charm fragmentation function [19].

Finally, we must divide by the number of $D^0$ mesons expected per $c\bar{c}X$ event: $f_{D^0} = 1.11 \pm 0.08$. This number is itself the product of four factors. The first is a factor of two to account for the two quarks, each of which may form a $D^0$. The next two factors account for all seven weakly-decaying $C = 1$ states $D^0, D^+, D_s, \Lambda_c, \Xi_c^+, \Xi_c^0$, and $\Omega_c^0$, relative to the measured $D^0$ yields. The fraction of $D^0$ compared to the total of $D^0 + D^+ + D_s + \Lambda_c, N(D^0)/[N(D^0) + N(D^+) + N(D_s) + N(\Lambda_c)] = 0.574 \pm 0.041$, is obtained from $e^+e^-$ fragmentation data [19]. An additional factor 0.98 ± 0.01 then accounts for the omitted $\Xi_c^+, \Xi_c^0$, and $\Omega_c^0$ states. This is estimated from the $\Lambda_c$ fraction of $N(\Lambda_c)/[N(D^0) + N(D^+) + N(D_s)]] = (8.1 \pm 2.1)$% in [19] (with an added uncertainty from knowledge of $\mathcal{B}(\Lambda_c \to pK\pi)$), combined with a theoretical suppression of order 10% due to the additional strange quark popping needed to form the omitted states. The fourth factor of 0.99 ± 0.01 accounts for charmonium states, which here include those states below open-flavor threshold at $\sqrt{s} = 2M_{D^0}: J/\psi, \psi(2S), \eta_c, \eta_c(2P), \chi_{cJ}, h_c$. We estimate $N(\text{open } c)/[N(\text{open } c) + 2N(\text{cc})] \approx 1 - 2N(\text{cc})/N(\text{open } c) \approx 1 - 2\mathcal{B}(c\bar{c}X \to \text{ charmonia})$ based on the production rate of $J/\psi$ in $e^+e^-$ fragmentation [20] and the branching fractions to charmonium in $\Upsilon(1S)$ decays [1]; these processes show that charmonium is rare in both $\gamma$ and $ggg$ hadronization. We are not sensitive to errors at the 1% level and choose a conservative uncertainty to accommodate unmeasured charmonium states. The various factors required for the six $\chi_{bJ}$ states are summarized in Table VI.

With these factors in hand, we fit our data for the $D^0X$ branching fractions with $p_{D^0} > 2.5 \text{ GeV}/c$ to the NRQCD predictions [9] and extract $\rho_8$, the ratio of color-octet to color-singlet matrix elements, in $\chi_{bJ}$ decays. Recall that both $f_2.5$ and $R_j^{(c)}$ depend on $\rho_8$ and that $f_2.5$ depends on fragmentation functions. For each value of $\rho_8$, we may convert our directly measured branching fractions into extracted values for $R_j^{(c)}$ in the context of this NRQCD calculation (which includes the assumption that $e^+e^-$ charm fragmentation data is representative of our charm fragmentation). The best value of $\rho_8$ is obtained from a fit which finds the best agreement between the predicted and extracted $R_j^{(c)}$. 
TABLE VI: Summary of factors used to relate our measured $D^0X$ branching fractions to $R_J^{(c)}$, which measures the total $c\bar{c}X$ rate. The values of $f_{2.5}$ are evaluated at the independently fitted best values of $\rho_8$ for each triplet.

| Factor | $\chi_{b0}(1P)$ | $\chi_{b1}(1P)$ | $\chi_{b2}(1P)$ | $\chi_{b0}(2P)$ | $\chi_{b1}(2P)$ | $\chi_{b2}(2P)$ |
|--------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $\mathcal{B}(\chi \to gg, q\bar{q}g)$ | 0.97 ± 0.03 0.65 ± 0.08 0.78 ± 0.04 | 0.93 ± 0.07 0.68 ± 0.04 | 0.75 ± 0.03 |
| $f_{2.5}$ | 0.54 | 0.70 | 0.63 | 0.45 | 0.46 | 0.47 |
| $f_{P^0}$ | 1.11 ± 0.08 1.11 ± 0.08 1.11 ± 0.08 1.11 ± 0.08 1.11 ± 0.08 1.11 ± 0.08 |
| $1/(f_{D^0}f_{2.5}\mathcal{B})$ | 1.70 ± 0.13 | 1.97 ± 0.28 | 1.83 ± 0.16 | 2.15 ± 0.23 | 2.89 ± 0.28 | 2.56 ± 0.21 |

We fit separate $\rho_8$ values for each triplet by minimizing a $\chi^2$ which has one term for each of the three states. Each term in the $\chi^2$ is formed from the square of the deviation of the predicted and extracted $R_J^{(c)}$ values, normalized by the errors on the extracted value. Note that both the predicted and extracted $R_J^{(c)}$ values depend on $\rho_8$. Correlated systematic uncertainties on the branching fractions are incorporated into the covariance matrix used to evaluate the $\chi^2$ in our fits. We find, however, that results are insensitive to correlations due to the dominance of statistical errors. The best-fit values are $\rho_8(1P) = 0.160^{+0.071}_{-0.047}$ and $\rho_8(2P) = 0.074^{+0.018}_{-0.008}$ with $\chi^2(1P) = 0.40$ and $\chi^2(2P) = 4.71$, respectively, for $3 - 1$ degrees of freedom each. The errors are larger for the $1P$ states primarily due to the non-linear dependence of the branching fractions on $\rho_8$: for larger $\rho_8$, the branching fractions are less sensitive to changes in its value.

It has been argued [21] that $\rho_8$ should be largely independent of radial quantum number. While we prefer not to assume such an equality, a joint fit to our branching fractions for both triplets obtains a best-fit common value of $\rho_8 = 0.086^{+0.009}_{-0.013}$, with $\chi^2 = 10.1$ for $6 - 1$ degrees of freedom.

Table VII lists the best-fit branching fractions, $R_J^{(c)}$, extracted from our data along with the best-fit NRQCD values, based on fits with separate $\rho_8$ parameters for each $\chi_{bJ}$ triplet. We also show the original 1979 calculations [6] for comparison. The third uncertainty is due to uncertainties in the branching fractions used to obtain $\mathcal{B}(\chi \to gg, q\bar{q}g)$ and the fragmentation data used to obtain $f_{P^0}$ and $f_{2.5}$. No systematic uncertainty is included for the accuracy of the theoretical calculations or the assumption that the $e^+e^-$ fragmentation data is a valid model for our charm fragmentation since we do not know how to quantify such effects. Thus, while our primary results for the inclusive $\chi_{bJ}$ branching fractions into $D^0X$ with $p_{D^0} > 2.5$ GeV/c are model-independent, our results for $R_J^{(c)}$ are clearly model-dependent.

IX. CONCLUSION

We report first measurements of the branching fractions for $\chi_{bJ}(1P, 2P) \to D^0X$ with $p_{D^0} > 2.5$ GeV/c. Our results are used to infer the total production of charm in $\chi_{bJ}$ decays, $R_J^{(c)}$ in the context of a recent NRQCD calculation [9]. The results are in agreement with this calculation, as well as the older calculations [6]. Notably, our $R_J^{(c)}$ values confirm that the largest branching fractions to charm correspond to the $J = 1 \chi_{bJ}$ states.
TABLE VII: Summary of extracted branching fractions (or upper limits) for $R_j^{(c)}$. NRQCD best-fit values use distinct $\rho_8$ values for each $\chi_{bJ}$ triplet. The original 1979 calculations [6] are also shown. The uncertainties are statistical, our systematic, and external systematic, respectively.

| State   | $R_j^{(c)}$ (%) | 90% CL UL (%) | NRQCD Best Fit (%) | Pred. from [6] (%) |
|---------|-----------------|---------------|--------------------|--------------------|
| $\chi_{b0}(1P)$ | $9.6 \pm 6.2 \pm 0.8 \pm 0.8$ | < 17.9 | 6.3 | 6 |
| $\chi_{b1}(1P)$ | $24.8 \pm 3.8 \pm 2.2 \pm 3.6$ | 23.7 | 25 |
| $\chi_{b2}(1P)$ | $9.8 \pm 3.5 \pm 0.9 \pm 0.9$ | < 14.6 | 10.8 | 12 |
| $\chi_{b0}(2P)$ | $8.7 \pm 6.4 \pm 0.9 \pm 0.7$ | < 17.7 | 4.9 | 6 |
| $\chi_{b1}(2P)$ | $25.3 \pm 4.3 \pm 2.5 \pm 2.4$ | 22.1 | 25 |
| $\chi_{b2}(2P)$ | $0.4 \pm 3.5 \pm 0.4 \pm 0.1$ | < 6.1 | 7.4 | 12 |

X. ACKNOWLEDGMENTS

We thank the authors of Ref. [9] for providing convenient parameterizations of their results. We gratefully acknowledge the effort of the CESR staff in providing us with excellent luminosity and running conditions. D. Cronin-Hennessy and A. Ryd thank the A.P. Sloan Foundation. This work was supported by the National Science Foundation, the U.S. Department of Energy, the Natural Sciences and Engineering Research Council of Canada, and the U.K. Science and Technology Facilities Council.

[1] W.-M. Yao et al. (Particle Data Group), J. Phys. G: Nucl. Part. Phys. 33, 1 (2006).
[2] C. Cawlfield et al. (CLEO Collaboration), Phys. Rev. D 73, 012003 (2006); D. Cronin-Hennessy et al. (CLEO Collaboration), Phys. Rev. Lett. 92, 222002 (2004).
[3] R. Barbieri, R. Gatta, and R. Kögerler, Phys. Lett. B 60, 183 (1976).
[4] H. Albrecht et al. (ARGUS Collaboration), Z. Phys. C 55, 25 (1992).
[5] H. Fritzsch and K.-H. Streng, Phys. Lett. B 77, 299 (1978).
[6] R. Barbieri, M. Caffo, and E. Remiddi, Phys. Lett. B 83, 345 (1979).
[7] G.T. Bodwin, E. Braaten, and G.P. Lepage, Phys. Rev. D 46, R1914 (1992).
[8] G.T. Bodwin, E. Braaten, and G.P. Lepage, Phys. Rev. D 51, 1125 (1995) [E: Phys. Rev. D 55, 5853 (1997)].
[9] G.T. Bodwin, E. Braaten, D. Kang, J. Lee, Phys. Rev. D 76, 054001 (2007).
[10] G. Viehhauser et al., Nucl. Inst. Meth. A 462, 146 (2001).
[11] D. Peterson et al., Nucl. Inst. Meth. A 478, 142 (2002).
[12] M. Artuso et al., Nucl. Inst. Meth. A 502, 91 (2003).
[13] Y. Kubota et al., Nucl. Inst. Meth. A 320, 66 (1992).
[14] S. Kopp et al. (CLEO Collaboration), Phys. Rev. D 63, 092001 (2001).
[15] M. Artuso et al. (CLEO Collaboration), Phys. Rev. Lett. 94, 032001 (2005).
[16] T. Skwarnicki, Ph.D. Thesis, Cracow Institute of Nuclear Physics, DESY-F31-86-02, 1986; J. Gaiser, Ph.D. Thesis, Stanford University, SLAC-255, 1982; R. Lee, Ph.D. Thesis, Stanford University, SLAC-282, 1985.
This number is based on the work described in M.E. Watkins, Ph.D. Thesis, Carnegie Mellon University, 2007 (unpublished), used here with a conservative error; it is also consistent with the predictions of D. Kang, T. Kim, J. Lee, C. Yu, Phys. Rev. D 76, 114018 (2007).

T. Sjöstrand et al., Computer Physics Commun. 135, 238 (2001).

R. Seuster et al. (Belle Collaboration), Phys. Rev. D 73, 032002 (2006).

K. Abe et al. (Belle Collaboration), Phys. Rev. Lett. 88, 052001 (2002).

N. Brambilla, D. Eiras, A. Pineda, J. Soto, A. Vairo, Phys. Rev. Lett. 88, 012003 (2001).