LONG-TERM TRANSIT TIMING MONITORING AND REFINED LIGHT CURVE PARAMETERS OF HAT-P-13b

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ABSTRACT

We present 10 new transit light curves of the transiting hot Jupiter HAT-P-13b, obtained during two observational seasons by three different telescopes. When combined with 12 previously published light curves, we have a sample consisting of 22 transit light curves, spanning 1041 days across four observational seasons. We use this sample to examine the recently observed large-amplitude transit timing variations (TTVs) by Pál et al. and give refined system parameters. We find that the transit times are consistent with a linear ephemeris, with the exception of a single transit time, from UT 2009 November 5, for which the measured mid-transit time significantly deviates from our linear ephemeris. The nature of this deviation is not clear, and the rest of the data do not show any significant TTVs.

Key words: planetary systems – stars: individual (HAT-P-13)

Online-only material: color figures, machine-readable and VO tables

1. INTRODUCTION

HAT-P-13 (Bakos et al. 2009) is among the brightest stars (V = 10.6 mag) hosting a multi-planet system containing a transiting planet, HAT-P-13b (Mp,b = 0.85 MJ, Rp,b = 1.3 RJ; Bakos et al. 2009; Winn et al. 2010). A transit depth of ~1% and a short orbital period of ~2.92 days allow for many transits that can be observed by small ground-based telescopes, making this system a good subject of observational studies related to planetary systems (e.g., Mardling 2010; Winn et al. 2010; Payne & Ford 2011).

HAT-P-13b was discovered as a transiting planet by Bakos et al. (2009), who also identified a second planet in the system, HAT-P-13c (Mp,c sin i,c = 14.3 MJ; Winn et al. 2010), moving in an eccentric orbit (e ≈ 0.7), with a period of about 1.2 years. Winn et al. (2010) gathered additional radial velocity (RV) measurements and identified a third low-mass companion in the system, possibly a third planet, whose period is currently unknown but expected to be a few years or longer. In addition, Winn et al. (2010) identified that HAT-P-13b’s orbit is likely to be aligned with the host star’s equator. As indicated by Winn et al. (2010), based on the analysis of Mardling (2010), a spin–orbit alignment of HAT-P-13b suggests a small mutual orbital inclination of planets b and c, suggesting in turn the possibility that planet c is also transiting. So far no transits of HAT-P-13c have been detected, although some attempts were made to look for this during the 2010 predicted conjunction time (Szabó et al. 2010).

In a recent paper, Pál et al. (2011) analyzed transit timing of HAT-P-13b from four observational seasons, 2007/2008 (hereafter Season 1), 2008/2009 (hereafter Season 2), 2009/2010 (hereafter Season 3) and 2010/2011 (hereafter Season 4), and identified a deviation of the transit times of about 0.015 days from the predicted times during the last season. In principle, this kind of long-term transit timing variation (TTV) could be due to the presence of another planet in the system in a large eccentric orbit as described, for example, by Agol et al. (2005, their Section 4). The known orbit of HAT-P-13c does not match the TTV pattern identified by Pál et al. (2011), but that could be due to the third planet suggested by Winn et al. (2010), or a further companion in the system.

We have set out here to study the suggested TTV signal in more detail. We present 10 new HAT-P-13b transit light curves, 5 from each of Seasons 3 and 4, and combine them with the 12 light curves that were available to Pál et al. (2011). Therefore, our analysis is based on a total of 22 transit light curves, either partial or complete, from four consecutive observational seasons, including a single light curve from Season 1 and 6–8 light curves per season for Seasons 2–4. Overall, our data span 1041 days. In Section 2 we describe how we obtained the new data and performed photometric processing, and in Section 3 we present our transit light curve analysis. We discuss our results in Section 4 and give a short summary in Section 5.

2. OBSERVATIONS

Our 10 new transit light curves of HAT-P-13b from Seasons 3 and 4 were obtained at three observatories. A brief description of the three telescopes and instruments used is given in the following paragraphs.

Fred Lawrence Whipple Observatory (FLWO): FLWO is located on Mount Hopkins, near Amado, AZ. We used the KeplerCam 4k × 4k Fairchild CCD486 mounted on the FLWO 1.2 m telescope. KeplerCam has a pixel scale of 0′′62 pixel−1 (2 × 2 binning), and a 23′1 × 23′1 field of view (FOV). All four new FLWO light curves, two from each of Seasons 3 and 4, were obtained in the SDSS-i′ filter. These observations were conducted with the telescope nominally in focus, but the optical characteristics of the telescope create a relatively large point-spread function (PSF). The seven light curves from the discovery paper (Bakos et al. 2009) were also obtained with the FLWO 1.2 m and KeplerCam, and here we used a similar setup.
Falkes Telescope North (FTN): FTN is located on Mauna Haleakala in Maui, HI. We obtained four light curves from LCOGT’s robotic 2.0 m telescope using the Spectral Instruments camera and a Pan-STARRS Z filter. The camera consists of a 4k × 4k Fairchild Imaging CCD with a pixel scale of 0.304 pixel−1 (2 × 2 binning) and an FOV of 10.5 × 10.5. Exposure times ranged from 6 s to 10 s and a slight defocus was applied to the telescope in order to project the PSF onto a larger number of pixels, prevent saturation and increase the open shutter time relative to the overall cycle time. Three light curves were obtained during Season 3 and one during Season 4.

Byrne Observatory at Sedgwick (BOS): BOS is located at the Sedgwick Reserve near Santa Ynez, CA. We obtained two transit light curves of HAT-P-13b, both during Season 4, using the RC Optics 0.8 m remotely operated telescope at BOS. This telescope is equipped with a Santa Barbara Instrument Group STL-6303E camera containing a 3k × 2k Kodak Enhanced KAF-6306E CCD with a pixel scale of 0.572 pixel−1 (2 × 2 binning) and a 14.7′ × 9.8′ FOV. We observed in the SDSS-i′ filter, and exposure times ranged from 50 s to 80 s depending on atmospheric conditions. Due to the smaller aperture and shorter readout time (~10 s) at BOS, no defocusing was applied.

At all observatories we gathered CCD images encompassing the target star HAT-P-13. The moderately populated field surrounding the target provided several stars of similar brightness within the FOVs, to be used as comparison stars in the photometric processing. All data were reduced using standard routines for bias subtraction, dark current subtraction (when necessary), and flat-field correction. We extracted light curves with PyRAF using aperture photometry by dividing the flux of the target star by the weighted summed flux of several comparison stars in each image. Julian dates of mid-exposure were recorded during the observations, and later converted to BJD_TDB using the tools described in Eastman et al. (2010).9 We optimized aperture sizes and the selection of comparison stars by minimizing the scatter of the resulting light curves, while iteratively removing 5σ outliers. A total of two photometric outlier data points were removed from the collection of all light curves. All 10 new light curves are shown in Figures 1 and 2, and are listed in Table 1.

In addition to the 10 new light curves we obtained for this work, we also re-analyzed 12 light curves available in the literature. Those include one light curve from Season 1 and six from Season 2, all from Bakos et al. (2009), two light curves presented by Szabó et al. (2010) from Season 3, and three light curves from Pál et al. (2011) from Season 4. We adopted the previously published light curves as they were presented in their respective papers, and we only redid the fits in this work. Table 2 lists all 22 transit light curves included in our analysis.

## 3. ANALYSIS

### 3.1. Analysis of All Available Data

Our light curve fitting was done using the Transit Analysis Package (TAP; Gazak et al. 2011). TAP utilizes Monte Carlo Markov Chains (MCMC) with the Metropolis–Hastings algorithm and a Gibbs sampler (e.g., Ford 2005, 2006; Holman et al. 2006; Collier Cameron et al. 2007; Burke et al. 2007). To account for possible temporally correlated noise (e.g., Pont et al. 2006) TAP uses the wavelet likelihood approach of Carter & Winn (2009). TAP has the ability to simultaneously fit 13 parameters: orbital period (P), mid-transit time (Tc), orbital inclination (i), orbital semi-major axis normalized by the host star’s radius (a/Rs), planet-to-star radii ratio (Rp/Rs), two limb-darkening coefficients (u1 and u2) for a quadratic limb-darkening law, orbital eccentricity (e), and longitude of periastron (ω). In addition, TAP fits a linear slope (S), to account for a possible linear trend with time during the transit, a flux normalization factor (N), and two noise components: a temporally uncorrelated Gaussian “white” noise (σw) and a time-correlated “red” noise (σr) (see Equations (32)–(34) of Carter & Winn 2009), where a power spectrum density of 1/f is assumed.

We determined limb-darkening coefficients11 by interpolating over the grids of Claret (2000, 2004) and fixed these parameters in the analysis. Since e and ω are not well constrained by light curves alone Gaussian priors were assigned to these parameters using the values from Winn et al. (2010): e = 0.0133 ± 0.0041, and ω = 210° ± 27°. Therefore, our model includes five parameters simultaneously fitted to all light curves (P, Tc, i, a/Rs, and Rp/Rs), and 22 sets of four parameters (S, N, σw, and σr) fitted individually to each light curve. We used jump rates of 25% for all free MCMC parameters, and ran 10 chains of 10⁵ steps each, discarding the first 10% of each chain before combining results of all chains. Each chain started from a different initial position 10σ away from the optimized parameter values. The best-fit values, and upper and lower 1σ errors for each parameter were determined by taking the median, 15.9, and 85.1 percentile values, respectively, of the resulting a posteriori probability distributions. In order to check the chains for non-convergence, we calculated the Gelman–Rubin statistic (Gelman et al. 2003; Ford 2006; Holman et al. 2006). The ratio of interchain variance to the intrachain variance was found to be within 10% of unity for each free parameter, giving no indication of non-convergence. Results of this analysis are shown in the bold row of Table 3, and we used those parameters for the overplotted model in Figures 1–3.

Table 2 includes parameters that indicate the quality of each light curve. The photometric noise rate (PNR) is defined as PNR = rms/√T, where the root mean square (rms) is derived from the light curve residuals at individual median of cycles (including exposure time and any dead time such as

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8 Located at: 34°687604, −120°390967, 500 m.
9 Online tool for HJD, UTC to BJD, TDB conversion; http://astroutils.astronomy.ohio-state.edu/time/hjd2bjd.html.
10 http://ifa.hawaii.edu/users/egazak/Ha/TAP.html
11 u1, y = 0.5162 u2, y = 0.2448, u1, r = 0.3971 u2, r = 0.2977, u1, i = 0.2922 u2, i = 0.3192, u1, v = 0.3208 u2, v = 0.3124, u1, z = 0.2441 u2, z = 0.3226.
Figure 1. Five new light curves obtained in this work during Season 3, plotted in chronological order starting from the top, and offset in relative flux for clarity. The residuals after model subtraction appear below in the same order. The best-fitting model, from the analysis of all light curves, is overplotted in black. All dates are UT at the start of observation.

(A color version of this figure is available in the online journal.)

readout time) per minute. Also listed are $\sigma_w$ and $\sigma_r$, as fitted by TAP.

3.2. Seasonal Analyses

We repeated this process treating the collection of all light curves from each of Seasons 2–4 as separate subsets in order to look for possible variations in the system parameters from season to season. The resulting system parameters determined from all light curves and the three seasonal analyses can be found in Table 3. The bottom line of the table lists the parameters from Bakos et al. (2009) for comparison.

3.3. Refined Ephemeris

We used the results from fitting all light curves in order to look for TTV and determine a refined ephemeris. To that end
we analyzed each light curve separately by allowing only the mid-transit time and the four light curve specific parameters ($S$, $N$, $\sigma_w$, and $\sigma_r$) to vary. The resulting mid-transit times for each transit event are listed in Table 4.

Once we determined the mid-transit times and the errors on those measurements, we then performed a linear least-squares fit for a linear ephemeris, including $P$ and a reference epoch $T_{c,0}$. Since we have some freedom in choosing the epoch for which $T_{c,0}$ is fitted, we chose it to be during Season 3, when the covariance between $P$ and $T_{c,0}$ is minimized, although we do not have a light curve of that specific transit event. The resulting parameters and their uncertainties are listed in the bold row of Table 3. We verified that the resulting $\text{cov}(P, T_{c,0})$ is small enough and can be neglected when propagating the error bars to future (or past) mid-transit times.

4. DISCUSSION

The transit times $O - C$ diagram showing the residuals from our linear ephemeris is presented in Figure 4, and the residuals are listed in Table 4 as time difference, in seconds, and also...
after dividing by uncertainty of the mid-transit times to show the significance of the difference. A close look at Figure 4 shows that there is only a single significant outlier (12.7 minutes, 5.2σ), the earlier of the two transit events obtained by Szabó et al. (2010) during Season 3, on UT 2009 November 5. The linear fit to the mid-transit times produced $\chi^2 = 45.57$ with 20 degrees of freedom (dof), and a reduced $\chi^2$ of $\chi^2_{\text{red}} = 2.28$. However, this value is highly affected by the $\sim 5\sigma$ outlier from the UT 2009 November 5 transit. If this single point is ignored we get $\chi^2 = 19.36$ with 19 dof, and $\chi^2_{\text{red}} = 1.02$, but the difference in the resulting fit is small ($T_c,0$ and $P$ changed by $-0.5\sigma$ and $0.1\sigma$, respectively). The rms of the $O-C$ residuals including the UT 2009 November 5 event is 211 s and 144 s without including that event.

Comparing our $O-C$ diagram to the one presented by Pál et al. (2011, see their Figure 2) shows a dramatic difference. Their figure shows that the mid-transit times of the three light curves they obtained, during Season 4, strongly deviate from a linear ephemeris, by about 0.015 days, or 3σ−18σ according to the mid-transit time uncertainties they provide. The linear ephemeris derived in Szabó et al. (2010) and adopted by Pál et al. (2011) was based only on the seven Bakos et al. (2009) transit times from Seasons 1 and 2 and the two from Szabó et al. (2010) from Season 3. Therefore, the UT 2009 November

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### Table 2

| Date (UT) | N_t | Cycle Time (s) | $\sigma_0$ (%) | $\sigma_r$ (%) | PNR (° minute$^{-1}$) | Transit Part (OIBEO) | Filter | Telescope | Reference |
|-----------|-----|----------------|----------------|---------------|---------------------|----------------------|--------|------------|-----------|
| Season 1: 2007/2008 |
| 2008 Apr 25 | −204 | 29 | 0.19 | 0.50 | 0.14 | E O i’ | FLWO 1.2 m | Bakos et al. (2009) |
| Season 2: 2008/2009 |
| 2008 Apr 6 | −137 | 29 | 0.13 | 0.41 | 0.10 | O I B i’ | FLWO 1.2 m | Bakos et al. (2009) |
| 2008 Nov 9 | −136 | 29 | 0.14 | 0.56 | 0.13 | O I B E O i’ | FLWO 1.2 m | Bakos et al. (2009) |
| 2008 Nov 12 | −135 | 29 | 0.18 | 0.13 | 0.18 | B E O i’ | FLWO 1.2 m | Bakos et al. (2009) |
| 2009 Jan 18 | −112 | 29 | 0.14 | 0.14 | 0.15 | O I B E O i’ | FLWO 1.2 m | Bakos et al. (2009) |
| 2009 Feb 19 | −101 | 29 | 0.18 | 0.55 | 0.14 | O I B i’ | FLWO 1.2 m | Bakos et al. (2009) |
| 2009 May 9 | −74 | 29 | 0.16 | 0.85 | 0.14 | O I B i’ | FLWO 1.2 m | Bakos et al. (2009) |
| Season 3: 2009/2010 |
| 2009 Nov 5 | −12 | 132 | 0.06 | 0.57 | 0.19 | O I B E O | R & V | Konkoly 1.0 m | Szabó et al. (2010) |
| 2009 Dec 28 | 6 | 23 | 0.17 | 0.29 | 0.11 | O I | Z | FTN 2.0 m | This work |
| 2009 Dec 31 | 7 | 22 | 0.22 | 0.58 | 0.15 | O I B | Z | FTN 2.0 m | This work |
| 2010 Jan 3 | 7 | 44 | 0.13 | 0.19 | 0.14 | O I B | i’ | FLWO 1.2 m | This work |
| 2010 Feb 4 | 19 | 30 | 0.12 | 0.46 | 0.12 | O I B E O | Z | FTN 2.0 m | This work |
| 2010 Feb 21$^a$ | 25 | 411 | 0.09 | 0.58 | 0.43 | O I B E O | R | Konkoly 0.6 m | Szabó et al. (2010) |
| 2010 Mar 20 | 34 | 34 | 0.15 | 0.38 | 0.12 | O I B | i’ | FLWO 1.2 m | This work |
| Season 4: 2010/2011 |
| 2010 Nov 11 | 115 | 39 | 0.16 | 0.53 | 0.14 | O I B E O | i’ | FLWO 1.2 m | This work |
| 2010 Dec 27 | 131 | 39 | 0.19 | 0.75 | 0.17 | O I B E O | I | Konkoly 0.6 m | Pál et al. (2011) |
| 2010 Dec 30 | 132 | 63 | 0.08 | 1.29 | 0.17 | O I B | R | Konkoly 1.0 m | Pál et al. (2011) |
| 2011 Jan 28 | 142 | 28 | 0.17 | 1.44 | 0.15 | O I B E | R | Konkoly 1.0 m | Pál et al. (2011) |
| 2011 Feb 21 | 150 | 31 | 0.27 | 0.55 | 0.23 | O I B E | Z | FTN 2.0 m | This work |
| 2011 Feb 24 | 151 | 62 | 0.10 | 0.19 | 0.11 | O I B | i’ | BOS 0.8 m | This work |
| 2011 Feb 27 | 152 | 94 | 0.11 | 0.37 | 0.15 | O I B E O | i’ | BOS 0.8 m | This work |
| 2011 Mar 2 | 153 | 34 | 0.11 | 0.65 | 0.10 | B E O | i’ | FLWO 1.2 m | This work |

### Notes

$^a$ UT date at start of observation.

$^b$ Photometric noise rate, calculated as rms/$\sqrt{T}$, where rms is the scatter in the light curve residuals and $\Gamma$ is the median number of cycles (exposure time and dead time) per minute.

$^c$ OIBEO for out-of-transit before ingress, ingress, flat bottom, egress, and out-of-transit after egress, respectively.

$^d$ The long cycle time (and resulting PNR) is the result of ignoring the V-band data of this event. Observations were originally taken while alternating between V and R filters, but the V-band data were plagued by large systematics and ignored in the analysis of Szabó et al. (2010).

### Table 3

| Data | $T_C,0$ (BJD TDB) | $P$ (days) | $i$ (deg) | $a/R_s$ | $R_p/R_s$ |
|------|-----------------|-----------|---------|---------|----------|
| All  | 2455176.53880 ± 0.00034 | 2.9162430 ± 0.000030 | 82.45 ± 0.46 | 5.52 ± 0.17 | 0.0855 ± 0.0011 |
| Season 2: 2008/2009 | 2454779.92895 ± 0.00072 | 2.916305 ± 0.000033 | 83.4$^{+1.0}_{-0.8}$ | 5.86$^{+0.41}_{-0.34}$ | 0.0838 ± 0.0019 |
| Season 3: 2009/2010 | 2455231.9464 ± 0.0012 | 2.915952 ± 0.000063 | 81.16 ± 0.70 | 5.00 ± 0.23 | 0.0882 ± 0.0020 |
| Season 4: 2010/2011 | 2455619.80708 ± 0.00085 | 2.916203 ± 0.000048 | 82.05 ± 0.93 | 5.37 ± 0.36 | 0.0857 ± 0.0021 |
| Bakos et al. (2009) | 2454779.92979 ± 0.00038 | 2.916260 ± 0.000010 | 83.4 ± 0.86 | 5.84 ± 0.26 | 0.0844 ± 0.0013 |
5 transit time from Season 3 heavily affected their derived ephemeris.

Here, we have seven events from Season 3, including three observed by the FTN 2.0 m and two by the FLWO 1.2 m. Our larger number of observed transits from that season suggests that the UT 2009 November 5 mid-transit time measurement is a single outlier, and that the data we have at hand are consistent with a linear ephemeris.

We present the light curve from the UT 2009 November 5 event in Figure 3, overplotted by our model from the analysis of all light curves and shifted to the best-fitting mid-transit time for the UT 2009 November 5 event (left), and the mid-transit time from the linear ephemeris (right). A close look at the light curve residuals, presented at the bottom part of both panels, shows that it includes a few features, specifically during and before ingress, and during and after egress, and these features are clearly more pronounced in the right panel. It is possible that those features have affected the estimate of the mid-transit time, and their origin could be astrophysical (although HAT-P-13 is not known to be an active star), or the result of correlated noise.

We carefully examined the UT 2009 November 5 light curve, which consists of exposures alternating between $V$ and $R$ filters. We measured the mid-transit time for the light curve observed in each filter independently, and found that they were both

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**Figure 3.** UT 2009 November 5 light curve, which was obtained by Szabó et al. (2010). Our best-fitting model obtained from TAP analysis of all 22 light curves is overplotted in black. Left: the model is phased and shifted to the best-fitting mid-transit time for this event. Right: the model is phased and shifted to the best-fitting linear ephemeris from Table 3.

(A color version of this figure is available in the online journal.)

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**Figure 4.** $O-C$ plot including all 22 mid-transit time measurements. The black dashed lines indicate the 1σ errors on the predicted mid-transit times by propagating the errors on $P$ and $T_{c,0}$ from the linear fit.

(A color version of this figure is available in the online journal.)
Table 4

Mid-transit Times of HAT-P-13b for the 22 Light Curves Analyzed Here

| \( N_{\text{tr}} \) | \( T_c \) | \( \sigma_T \) | \( O-C \) | \( O-C/\sigma_T \) |
|---|---|---|---|---|
| 0 (BJD_TDB) | (s) | (s) | |
| 204 | 2454581.625065 | 165 | −13 | −0.08 |
| 137 | 2454777.012591 | 106 | −79 | −0.74 |
| 36 | 2454779.930096 | 83 | 30 | 0.36 |
| 135 | 2454783.843600 | 197 | 206 | 1.05 |
| 112 | 2454849.920092 | 110 | 44 | 0.40 |
| 101 | 2454882.000478 | 204 | 192 | 0.94 |
| 74 | 2454960.739683 | 283 | 248 | 0.88 |
| 12 | 2455141.552706 | 146 | 762 | 5.22 |
| 6 | 2455194.035662 | 198 | −51 | 0.26 |
| 7 | 2455196.945496 | 110 | 173 | 1.57 |
| 8 | 2455199.868674 | 113 | −6 | −0.05 |
| 19 | 2455231.945420 | 79 | −172 | −2.18 |
| 25 | 2455249.447554 | 171 | 232 | 1.36 |
| 34 | 2455275.691211 | 230 | 178 | 0.78 |
| 115 | 2455511.908538 | 122 | 155 | 1.27 |
| 131 | 2455558.563744 | 146 | −249 | −1.71 |
| 132 | 2455561.486338 | 269 | 66 | 0.25 |
| 142 | 2455590.644415 | 222 | −76 | −0.34 |
| 150 | 2455613.973903 | 194 | −116 | −0.60 |
| 151 | 2455616.892899 | 131 | 122 | 0.93 |
| 152 | 2455619.807862 | 116 | 11 | 0.10 |
| 153 | 2455622.731514 | 143 | −39 | −0.28 |

within 1.3σ of the mid-transit time that we measured from the combined light curve, and close to 4σ away from the linear ephemeris. We then applied a completely separate analysis of the combined light curve from both filters in which the parameters that determine the shape of the light curve \((i.e., a/R_*, R_p/R_*, \text{ and } T_c)\) were fitted and allowed to vary freely. The resulting fitted parameters obtained from the analysis of this single event are within 1.3σ from the values obtained from the Season 3 analysis.

We verified that the mid-transit times we derived here for the transits observed by Bakos et al. (2009) and Pál et al. (2011) are consistent, within 0.7σ, with the times derived by those authors. We measure a mid-transit time of \(T_{c,n} = −12 = 2455141.552706 \pm 0.001700\) for the UT 2009 November 5 transit from Szabó et al. (2010) which is consistent with the value that they derive to within 0.3σ. Our value of \(T_{c,n} = 25 = 2455249.447554 \pm 0.001900\) for the second transit obtained by Szabó et al. (2010) from UT 2010 February 21 differs from the published value by 1σ.

As already noted, the source of the large-amplitude shift in the transit timing of the UT 2009 November 5 event is unclear, and since our data do not include other transit events near that time it is difficult to rule out or confirm a physical process. If of astrophysical origin, it could be the result of an unusual physical process that also affected the shape of the light curve (see Figure 3) which is not seen during the other transit events analyzed here. HAT-P-13b transits observed by others close to that event during 2009 October and November would be useful for shedding light on this issue.

We have attempted to look for a TTV signal in our \(O-C\) diagram, although it does not show an excess scatter, besides the single outlier mentioned above. A parabolic fit to all 22 mid-transit times resulted in a value consistent with zero within 1σ for the quadratic coefficient, and with \(\chi^2 = 43.62\) for 19 dof, or \(\chi^2_{\text{red}} = 2.30\). Ignoring the UT 2009 November 5 outlier gives \(\chi^2 = 19.31\) for 18 dof, or \(\chi^2_{\text{red}} = 1.07\), and the rms of the \(O-C\) residuals are 210 s including the UT 2009 November 5 event and 144 s without that event. Therefore, we could not identify a long-term trend in the transit times.

We also performed a period analysis on the residuals from the linear ephemeris using the Lomb–Scargle method (Lomb 1976; Scargle 1982), looking for a possible low-mass perturber (e.g., Holman & Murray 2005). The maximum peak of the periodogram was found to be similar to the maximum peak of periodograms in which the data were rearranged in a random order. More quantitatively, the strongest periodogram peak was at the 52nd percentile of a sample of strongest peaks in periodograms of 104 random permutations, showing that no significant periodicity is seen in our mid transit times \(O-C\) residuals. The large outlier from the UT 2009 November 5 event of Szabó et al. (2010) was not included in this L-S analysis.

Several authors have presented predicted TTV behavior of HAT-P-13b transits (Bakos et al. 2009; Payne & Ford 2011), depending on the parameters of the second planet, HAT-P-13c. Our data put an upper limit on the maximum TTV amplitude of \(\sim 150\) s during the four observational seasons. This reinforces the claim of Payne & Ford (2011) that the eccentricity of the outer planet must be less than \(\sim 0.85\), and the relative inclinations of the two planet’s orbital planes must not be in the range 88° < \(i_{\text{rel}}\) < 92°.

Of course it could be that there is yet another, short-period low-mass planet lurking in the system. To that end we note that a \(\sim 3\) Earth mass planet orbiting at a coplanar orbit with twice the orbital period of HAT-P-13b will induce a TTV amplitude of \(150\) s (Pál 2010), close to the detection threshold of our data. However, such a planet will also induce a 1 m s⁻¹ RV amplitude. Therefore, the sensitivity of our transit timings to non-transiting planets in a 1:2 resonance is close to that of existing RV data (Bakos et al. 2009; Winn et al. 2010).

Our Season 2 light curves include data only from Bakos et al. (2009). Comparing our results for that season with the parameters presented by Bakos et al. (2009) shows they are in good agreement and are consistent within 0.5σ (see Table 3). This is an important validation of our analysis method using the TAP software. The uncertainties we derive are larger, though, by typically 40%–60%, and 330% for the orbital period. The latter can be explained by the additional value of the HATNet photometry in constraining the period, but the former may indicate that our uncertainties are overestimated and/or those of Bakos et al. (2009) are underestimated. The error bars are also influenced by the fact that we did not include the UT 2008 April 25 event in the Season 2 analysis, since it was obtained during Season 1, although that light curve is partial and has a small impact on the parameters’ uncertainties.

Thanks to our large amount of data with a much longer time span the errors on the system light curve parameters from the analysis of all 22 light curves are smaller than those obtained by Bakos et al. (2009) by 15%–35%, and more than a factor of three smaller for \(P\).

Our separate analysis of the data from each season (see Table 3) shows a small shift of \(\sim 2.5\sigma\) in \(i, a/R_*, \text{ and } R_p/R_*\) from Season 2 to Season 3, while the results for Seasons 3 and 4 are consistent within 1.2σ. The transit duration also shows a jump of \(\sim 2.8\sigma\) between Season 2 and Season 3, but the duration for Season 2, Season 4, and all 22 light curves is consistent to within 0.5σ. The shift in Season 3 may be influenced by the UT 2009 November 5 event, as the light curve (see Figure 3) of
this event may indicate a longer duration than other transits in our collection of data. The low significance of those shifts and the fact that these parameters are correlated makes it difficult to draw any conclusion. If the UT 2009 November 5 light curve is excluded from the Season 3 analysis, then this jump becomes slightly less significant. The values of $i$, $a/R_s$, and $R_p/R_s$ ($i = 81.67 \pm 0.87$, $a/R_s = 5.29 \pm 0.31$, $R_p/R_s = 0.0858 \pm 0.0023$) if the UT 2009 November 5 event is excluded are consistent with the values of Season 3 when that event is included to within 0.4$\sigma$, and are less than 2$\sigma$ away from Season 2.

5. SUMMARY

We presented here an analysis of 22 HAT-P-13b transit light curves spanning four observational seasons, of which 10 were obtained here and 12 were previously published. Contrary to the long-term TTV signal suggested by Pál et al. (2011) we find that the transit times are consistent with a linear ephemeris, while we identify a single transit time, from UT 2009 November 5, that significantly deviates from our linear model. The nature of this single deviation is unclear. The other light curve parameters do not show a large deviation compared to those fitted to light curves of the same season. Our large data set also allows us to refine the light curve parameters and transit ephemeris, which will be useful for future observational studies of this interesting system.

This work demonstrates the use of a collaboration of ground-based 1 m class telescopes for transit timing monitoring, and that a large number of observations are required for thoroughly studying any TTV detection. This will undoubtedly be one of the goals of the future robotic 1 m class telescope networks, like LCOGT (e.g., Shporer et al. 2010). Unlike expensive space missions as CoRoT and Kepler, small ground-based telescopes are easily accessible and their lifetime is not limited by the durations of space missions. Therefore, they will be an important resource in studying transiting planets orbiting bright stars in the decades to come.

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Facilities: FTN (Spectral), FLWO:1.2m (KeplerCam), LCOGT (BOS)

Note added in proof. After the submission of this work, Nascimbeni et al. (2011) appeared on arXiv. The five new light curves from Season 5 presented in that work are critical to ruling out a nonlinear ephemeris.

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