Abstract: Changes in the structure and sizes of human and bovine serum albumins as well as polyvinyl alcohol macromolecules in aqueous solutions depending on temperature, concentration, and acid-base balance (pH) of the solutions are discussed. It is taken into consideration that the change in the hydrodynamic radius of a macromolecule is one of the indicators of structural phase transformations of globular proteins. The methods of the macromolecular radii determination from the shear viscosity and the self-diffusion of macromolecules in solutions are discussed. The hydrodynamic radius values of albumin and polyvinyl alcohol macromolecules obtained by the above methods are thoroughly compared. Consideration of these questions provides us with important information on the nature of the binding of water molecules with protein macromolecules.

Keywords: macromolecular sizes; human serum albumin; bovine serum albumin; aqueous solutions

1. Introduction

The structure and properties of proteins continue to be in the focus of attention of physicians, chemists, physicists, and other researchers. Features of changes in the protein structure, being dissolved in water and aqueous solutions, are the main research questions for physicists [1]. Herein we want to dwell on transformations that occur with albumin macromolecules in solutions. In this article we will focus on the macromolecules of human serum albumin (HSA) and bovine serum albumin (BSA).

Human serum albumin (HSA) consists of 585 amino acid residues combined into a single macromolecular chain with a molecular weight of 66.5 kDa [2]. In the crystalline state, the HSA macromolecule is folded into a compact conformation of a heart-shaped regular triangular prism with...
sizes of ~80 Å and ~30 Å [3]. Bovine serum albumin (BSA) consists of 583 amino acid residues combined into a macromolecule with a molecular weight of 66.5 kDa and a spatial structure similar to that of HSA [2,4]. The amino acid sequences of HSA and BSA are 75.52% identical [5].

The domain structure of HSA and BSA is generally accepted. At physiological pH values, the secondary structure of HSA and BSA consists of alpha helices (50–68%) and beta folds (16–18%) stabilized by hydrogen bonds, as well as an unordered part of the macromolecular chain [2,4,6]. Due to 17 disulfide bonds between the cysteine residues of the alpha helices, the tertiary structure of these albumins is formed: three domains are formed, each of which is formed by subdomains of three alpha helices, and hydrophobic interactions between the domains determine the globular structure of proteins [2,4].

Differences in the nucleotide sequences of albumins lead to some change in the hydrophobicity and conformational mobility of the HSA macromolecule compared to the BSA macromolecule [5]. One of the differences in the HSA structure is the presence of two tryptophan residues (Trp134 and Trp213) in the BSA macromolecular sequence, in contrast to one tryptophan residue in the HSA macromolecule (Trp214) [2].

When dissolved in water, as well as in aqueous and biological solutions due to interaction with water, the rigid conformation of albumin macromolecules should violate. To the greatest extent, this applies to those structural features of albumin that are due to Coulomb forces. Upon dissolution, a slight redistribution of locally charged sections of the albumin macromolecule occurs, which changes its hydrophilic and hydrophobic properties. The latter can be the cause of compaction of albumin macromolecules, i.e. reduction in the size of the macromolecule, while the predominance of hydrophilic interactions can contribute to the transformation of a quasi-linear structure into a compact domain structure [2,5]. Therefore, both hydrophobic and hydrophilic interactions can contribute to the destruction of the domain structure of albumin in solution, which is inherent in the crystalline state of a protein.

The dissolution of albumin macromolecules in water can be considered as an internal structural phase transition. The structural transformations of the albumin macromolecule will also change the structure of the water environment [7,8]. One of the features of such a phase transition is a change in the size of the macromolecule.

One of the indicators of the structural phase transformations is the hydrodynamic radius change. The latter is studied by various physicochemical methods: dynamic light scattering [9–11], small-angle neutron scattering [12–14], atomic force microscopy [15], small-angle X-ray scattering [16], pulsed-field gradients NMR spectroscopy [17,18], gel permeation chromatography [19], capillary viscometry [20].

We focused on methods that allow us to determine the radius of albumin macromolecules as an indicator of conformational transitions using the shear viscosity of macromolecular solutions and the self-diffusion coefficients of macromolecules in them. These methods allow 1) to study the change in the hydrodynamic radius of the macromolecule depending on temperature, concentration, acid-base balance (pH), the presence of salts and the nature of the buffer solutions; 2) to analyze the dynamics of solvent molecules associated by intermolecular interactions with a macromolecule.

To differentiate the temperature, concentration, and acid-base balance (pH) effects on the internal structure of a macromolecule, a comparison is made of the temperature-concentration dependences of the hydrodynamic radius of albumin macromolecules and polyvinyl alcohol (PVA) macromolecules. It is important to note that the PVA macromolecule has an internally disordered,
statistically determined structure of the macromolecular coil in solution, while the internal structure of albumin has a strictly determined domain structure of the macromolecular globule, determined by the amino acids sequence.

The macromolecular radius dependence on the conformation changes of albumin macromolecules forms a separate problem and provides a basis for the next step—the study of changes of the macromolecular radius versus solution acid-base balance, which is one of the factors of conformation changes in proteins. At present, the concentration and temperature dependencies of the macromolecular radius of albumin at constant pH values have been obtained, which correlate well with the data obtained by other experimental methods.

2. Calculation method

2.1. Determination of the macromolecular radii from the shear viscosity of aqueous solutions

Here, the ratio between weight concentration $c_m$ and volume concentration $\varphi$ in the solution of macromolecules:

$$\varphi = \frac{4\pi R^3 c_m \rho N_A}{3M}$$  \hspace{1cm} (1)

where $R$ is the macromolecular radius; $\rho$ is the solution density; $N_A$ is the Avogadro constant; $M$ is the molecular weight of a substance. Hence, the effective radius of the macromolecule is determined by the ratio:

$$R = \gamma \varphi^{1/3}, \quad \gamma = d (\rho c_m)^{-1/3}, \quad d = \frac{3M}{4\pi N_A}$$  \hspace{1cm} (2)

where the mass density is determined by a linear combination:

$$\rho = \rho_w (1 - c_m) + \rho_{alb} c_m$$  \hspace{1cm} (3)

where $\rho_w$ is the mass density of water, $\rho_{alb}$ is the mass density of the crystalline albumin. For albumin macromolecules $d_{alb} = 2.98 \cdot 10^{-8} \text{kg}^{1/3}$.

With certain reservations macromolecules in dilute solutions can be approximated as spherical particles. In this assumption, the average viscosity of the dilute solution can be estimated from Einstein’s theory [21]:

$$\bar{\eta} = \eta_0 \left(1 + \frac{5}{2} \varphi \right)$$  \hspace{1cm} (4)

where $\eta_0$ is the solvent (water) viscosity, $\varphi$ is the volume concentration of macromolecules. The linear dependence of shear viscosity on volume concentration indicates neglect of hydrodynamic interaction between macromolecules.
It follows from equation (4) that $\varphi = \frac{2}{5} \lambda$, where $\lambda = \frac{\overline{\eta}}{\eta_0} - 1$, and for the effective radius of the macromolecule, considered as a function of excess viscosity, we find:

$$R_\eta = \gamma (0.4 \lambda)^{1.3}$$  \hspace{1cm} (5)

As shown in [22], formula (5) is only applicable to volume concentrations of $\varphi < 0.1$.

Hydrodynamic interactions between macromolecules become essential as the solution concentration increases. Their accounting was first performed by Batchelor [22], who proposed the formula:

$$\overline{\eta} = \eta_0 (1 + a_1 \varphi + a_2 \varphi^2 + ...)$$  \hspace{1cm} (6)

Where

$$a_1 = 2.5, \quad a_2 = 5.2$$  \hspace{1cm} (7)

By rewriting equation (6) in the form

$$a_1 \varphi + a_2 \varphi^2 + ... = \lambda,$$  \hspace{1cm} (8)

we’ll look for $\varphi$ as an endless series of degrees for $\lambda << 1$,

$$\varphi(\lambda) = b_1 \lambda + b_2 \lambda^2 + ...$$  \hspace{1cm} (9)

The first coefficients of this series take values:

$$b_1 = \frac{1}{a_1} = 0.4, \quad b_2 = \frac{a_2}{a_1^2} = -0.3328$$  \hspace{1cm} (10)

By substituting the values of $\varphi$ obtained in this way, we find:

$$R_\eta = \gamma (b_1 \lambda)^{1/3} \left[ 1 + \frac{b_2}{3 b_1} \lambda - \frac{1}{9} \left( \frac{b_2}{b_1} \right)^2 \lambda^2 + ... \right]$$  \hspace{1cm} (11)

where

$$\frac{b_2}{3 b_1} = -0.2773, \quad \frac{1}{9} \left( \frac{b_2}{b_1} \right)^2 = 0.0769$$  \hspace{1cm} (12)

Batchelor formula generalizes Einstein formula and turns out to be applicable up to volume concentrations $\varphi \leq 0.2$, which corresponds to the viscosity ratio: $\overline{\eta}/\eta_0 < 1.5$. Unfortunately, a
The further generalization of the Batchelor method faces considerable difficulties in finding the higher-order members of the perturbation theory, finding the sum of the series, and even in solving the question of its convergence.

The progress in determining the effective radii of macromolecules is associated with the use of cellular approaches [23], which take into account that hydrodynamic disturbances caused by macromolecular particles are localized mainly within a spherical cell that surrounds the particle. It is also considered that at the cell boundary the normal component of the perturbation rate and the tangential stress components are equal to zero, which is equivalent to the absence of friction on the outer cell surface [23]. Among different versions of cellular approaches, we give preference to the version [23,24], in which the neighboring macromolecules disturb the hydrodynamic field of the rotating particle. In this case, the properties of symmetry of the inoculum hydrodynamic field and the perturbed hydrodynamic field are used as fully as possible. Works [23,24] show that the viscosity of dilute solutions of macromolecules is determined by the formula:

\[
\eta = \eta_0 \frac{\psi(1-\psi)}{\psi(1-\psi) + 1 - \sqrt{1 + 2\psi^2(1-\psi)}} \tag{13}
\]

where \(\psi = (R_0/R)^3\), \(R_0\) is the macromolecule radius, and \(R\) is the cell radius. Thus, the task of determining the average viscosity of the macromolecule solution is reduced to establishing the relationship between the model parameter \(\psi = (R_0/R)^3\) and the value of specific volume \(\varphi = V_0/V\) measured experimentally, where \(V_0\) is the total volume occupied by macromolecules, and \(V\) – the volume of the liquid system. Formula (13) allows us to describe the viscosity behavior of dilute solutions of macromolecules up to the values of the volume concentration of \(\varphi \leq 0.5\), which actually coincides with the solution density corresponding to the direct contact of all the nearest neighbors [23,24]. It is important to note that at concentrations of \(\varphi \leq 0.2\) the formulas (13) and (6) are fully equivalent (this fact follows directly from the construction (13)).

We use equation (13) to determine the effective volume concentration:

\[
\overline{\varphi}_{\text{exp}} = \eta_{(13)}(\varphi) \tag{14}
\]

The effective radius of macromolecules is found directly by the formula (2). An independent method for determining the effective radius of macromolecules is related to their self-diffusion coefficient.

2.2. Evaluation of macromolecule radii from the self-diffusion coefficient of macromolecules in solution

The dependence of the self-diffusion coefficient on the volume concentration \(\varphi\) is usually presented in the form:

\[
D_3 = D_0 \left(1 + f(\varphi)\right) \tag{15}
\]

where
\[ D_0 = \frac{k_B T}{6\pi \eta_0 R_0} \] (16)

is the self-diffusion coefficient of a macromolecule in an extremely dilute solution. The same is also represented in another view:

\[ D_s = \frac{k_B T}{6\pi \eta_0 R_D} \] (17)

where \( R_D \) has meaning of the effective radius for a macromolecule. In the case of \( \varphi << 1 \) it can be represented in the form:

\[ R_D = R_0 + \delta R \] (18)

To define \( \delta R \) value, let us present the left part of equation (15) as a degree gradation of \( \frac{\partial R}{R_0} \) and the right part as a degree gradation of \( \varphi \). In this way we come to the equation:

\[ -\frac{\partial R}{R_0} + \frac{\partial R^2}{R_0^2} + \ldots = a_1 \varphi + a_2 \varphi^2 + \ldots, \quad a_1 = \frac{\partial f(\varphi)}{\partial \varphi} \bigg|_0, \quad a_2 = \frac{1}{2} \frac{\partial^2 f(\varphi)}{\partial \varphi^2} \bigg|_0, \quad \ldots \] (19)

As before, we’re looking for his solution in the form: \( \delta R / R_0 = b_1 \varphi + b_2 \varphi^2 + \ldots \) Equating the coefficients at the same degrees of \( \varphi \), we find:

\[ \delta R = R_0 \left[-a_1 \varphi + (a_1^2 - a_2) \varphi^2 + \ldots\right] \] (20)

In case of the linear nature of the function \( f(\varphi) : f(\varphi) = a \varphi + O(\varphi^2) \), the effective radius of the macromolecule is changed in the simplest way:

\[ R_D = R_0 (1 - a \varphi + \ldots) \] (21)

Recall that the above solutions for the effective radius of the macromolecule are fair for volume concentrations of \( \varphi \leq 0.5 \).

If the dependence of the self-diffusion coefficient on the volume concentration \( \varphi \) is presented in the form of equation (15), where \( \varphi \) turns out to be significantly different from zero, then the application of perturbation theory is unacceptable.

In this case we represent \( R_D \) as \( R_D = R_0 + \delta R \equiv R_0 (1 + u) \). Then

\[ D_\delta = D_0 \frac{1}{1 + u} \] (22)

and

\[ \varphi = \varphi_0 (c)(1 + u)^3 \] (23)

AIMS Biophysics

Volume 7, Issue 4, 219–235.
where \( \varphi_0(c) = (R_0/\gamma)^3 \). By substituting (22) and (23) in (15), we obtain the following equation for \( u \) determining:

\[
\frac{1}{1+u} = 1 + \lambda \varphi_0(1+u)^3
\]

(24)

where \( f(\varphi) \) is the known function of \( \varphi \).

3. **Results and discussion**

In this part, we will consider the successively effective hydrodynamic radii of polyvinyl alcohol (PVA), bovine serum albumin (BSA), and human serum albumin (HSA) macromolecules. In comparison with the latter two, PVA macromolecules have the simplest internal structure, which boils down to a sufficiently dense spherical core and a relatively rarefied periphery. It is assumed that the dense PVA core has a dominant influence on the shear viscosity behavior of its solutions. In the case of BSA and HSA, the character of temperature and temperature dependence of the effective hydrodynamic radius is complicated by the influence of their more complex internal structure. Our results on the size of albumin macromolecules refer to the temperature range up to 318 K, which corresponds to the stage of pre-denaturation of protein macromolecules.

3.1. **Evaluation of macromolecule radii from the self-diffusion coefficient of macromolecules in solution**

This section presents the results of the effective hydrodynamic sizes investigation of polyvinyl alcohol (PVA) macromolecules in aqueous solutions [25]. The PVA of Mowiol 6–98 (Kuraray) brand with the average molecular weight \( \bar{M}_w = 47 \text{kDa} \) that corresponds to the average number of monomers in a macromolecule \( p = 1000 \) and the concentration of OH-groups \( h = (98.4 \pm 0.4) \text{ mol.\%} \) in a macromolecule was used.

From the small-angle X-ray scattering [26–28] it follows that in the condensed state PVA has a flat zigzag-shaped configuration of the macromolecular chain with a period of identity equal to 2.52 Å. When dissolved in water, the macromolecular chain of PVA takes the conformation of the macromolecular coil [29]. Intramolecular hydrogen bonds in PVA macromolecule are stronger than hydrogen bonds between water molecules: \( \varepsilon_{ii}^{(pp)}/k_B T = -15.2 \) and \( \varepsilon_{ii}^{(pp)}/k_B T = -12.3 \) [30,31]. Therefore, the PVA macromolecule in dilute aqueous solutions gets the conformation of a sufficiently dense macromolecular coil [32–37]. The compactization of PVA macromolecular coil in aqueous solution is also due to hydrophobic effects [38,39].

Temperature and concentration dependencies of the effective radius of PVA macromolecules are restored by experimental values of shear viscosity of aqueous solutions from [25] according to formulas (14), (15), and (2) corresponding to the cell approach [22–24]. The results obtained in this way are presented in Figure 1.
As we can see, with increasing temperature and concentration, the effective hydrodynamic radius of a core $R_q$ decreases. Our neglect of the periphery influence on the solution viscosity is confirmed by the analysis performed in [40] by the molecular dynamics method. In this work it is shown that the shape of PVA macromolecule in aqueous solution is close to a spherical one with weakly blurred borders.

The concentration dependencies on temperature, at which the PVA macromolecule radius remains unchanged, were studied in [25]. These lines are characteristic curves that allow tracking the role of the effects of the interaction of macromolecules with solvent and among themselves at the overlap of their edges, as well as the disorder that increases with increasing temperature. Two straight lines intersecting at temperature $(315 \pm 2)$ K approximate the characteristic curves for aqueous PVA solutions [25]. As shown in [41,42] there is a dynamic phase transition in pure water at this temperature, when a significant change in the character of thermal motion of water molecules occurs. Thus, PVA macromolecules in aqueous solutions are indicators of changes in water properties [43,44].

The results obtained by us specify those given in other publications. In [45], the hydrodynamic radius of a macromolecule $R_d^{(PVA)} = 54.0$ Å was obtained from sedimentation coefficients at centrifugation of aqueous PVA solutions ($\overline{M}_w = 44$ kDa, $h = 88$ mol.%), which is slightly less than the value of 65 Å for dilute PVA solutions calculated by us. Some discrepancies of hydrodynamic radii can be explained by the different number of hydroxyl groups ($h$) in the investigated PVA macromolecules. According to the conclusions of the work [33], with a decrease in the content of hydroxyl groups in a macromolecule, the hydrodynamic radius of PVA macromolecules in aqueous solution decreases due to an increase in the packing density of macromolecule, caused by an increase in the number of hydrophobic interactions between acetate groups and water molecules.

In work [46] by the dynamic light scattering method the $R_d$ values for PVA aqueous solutions with the average number of monomers in a macromolecule $\overline{p} = 500$, 2000, 4000, and 8000 were received. Estimating $R_d$ on their basis for $\overline{p}=1000$, we receive $R_d^{(PVA)} = 9.6$ Å. The close to it
value of hydrodynamic radius \( R_{h}^{(PVA)} = 76 \, \text{Å} \) of PVA macromolecules \( \bar{M}_w = 38 \text{kDa}, \theta = 97.5 \text{ mol \%} \) is obtained from viscosity data on the basis of the Flory approach [46]. This value, corresponding to \( c = 0.01 \text{ wt \%} (\varphi = 0.02) \) at temperature \( T = 298 \text{ K} \), is close to the size of an ideal polymer chain \( R_i = r_0 N^{1/2} \).

Deviation from our calculated value of 65 Å for diluted PVA solutions may be caused by ignoring the additives specified by us (see equations (21)–(24)). Moreover, viscosity values lead to the size of the dense core, which is slightly smaller than the size of the PVA macromolecule with consideration of the rarefied periphery.

The results of work [47] testify to the growth of the hydrodynamic radius of macromolecules with temperature growth, which is also predicted in [39] using the method of molecular dynamics. Presented on Figure 1 surface of effective radius of PVA macromolecules in aqueous solutions shows constancy of effective radius of macromolecules up to concentrations \( \varphi \sim 0.2 \) and temperatures \( T \sim 330 \text{ K} \). Growth of fluctuations in the peripheral part of the macromolecule with temperature growth should lead to the increase in the periphery size. At the same time, the core size decreases or remains unchanged (see Figure 1).

### 3.2. Effective radii of bovine serum albumin macromolecules

To obtain effective radii of BSA macromolecules, we use experimental values of shear viscosity of BSA aqueous solutions obtained in [48]. Using equations (13), (14), and (2) of the cell approach we obtained temperature and concentration dependences of an effective radius of BSA macromolecules. The surface of effective radius of BSA macromolecules in the concentration range \((2.0 \div 20.0) \text{ wt.\%} (\varphi = (0.05 \div 0.49))\) and temperatures \((278 \div 318) \text{ K}\) at constant \( \text{pH} = 5.2\), corresponding to the vicinity of isoelectric point of BSA is presented in Figure 2.

As we can see, at all temperatures studied, the concentration dependencies of the effective radius of BSA macromolecules \( R_{h}^{(BSA)} \) are essentially not monotonous. At concentrations of \(~5 \text{ wt.\%} (\varphi \approx 0.17)\) the \( R_{h}^{(BSA)} \) values take maximum values and fall quickly enough in both directions from the maximum. At concentrations greater than \(10 \text{ wt.\%} (\varphi \approx 0.32)\), the concentration dependencies are quasi-linear.

The observed concentration maximum of effective radii \( R_{h}^{(BSA)} \) dependencies corresponds to isolated macromolecules since the transition from isolated macromolecules to macromolecules with overlapping peripheries occurs at the vicinity of 7 wt.\% \( (\varphi \approx 0.23) \) [38]. The maxima position of the effective radius \( R_{h}^{(BSA)} \) is in the physiological range of albumin concentrations (35–55 mg/ml) in plasma [48] and corresponds to the largest surface area of a macromolecule. In its turn it provides maximum access to albumin binding centers for performing one of its main functions—the transport one [2,49–51].
Figure 2. Temperature and concentration dependence of effective radii of bovine serum albumin macromolecules at pH value 5.2 [48].

Figure 3. Concentration dependence of effective BSA radii in aqueous solutions at \( T = 298 \text{K} \) and pH = 5.2 [48].

Let us compare the sizes of BSA macromolecules obtained from the analysis of shear viscosity of its aqueous solutions with the available literature data. In [52] the dynamic light scattering for dilute BSA aqueous solutions (temperature \( T = 298 \text{K} \), acid-base balance pH = 5.0, the concentration of ions \( I = 0.15 \) M) was used to determine the self-diffusion coefficient \( D_s = (6.14 \pm 0.03) \times 10^{-11} \text{m}^2/\text{s} \), which using equations (17) and (21) leads to \( R_D^{(\text{BSA})} = (39.92 \pm 0.03) \text{Å} \). This value practically coincides with 39.90 Å obtained from the analysis of viscosity at \( c_m = 2.14 \) wt.% (\( \varphi = 0.06 \)), \( T = 298 \text{K} \), pH = 5.2. It should be emphasized that the pH of solutions in both compared cases is close to the isoelectric point of BCA solutions.

The method of dynamic light scattering to determine the values of self-diffusion coefficient of albumin macromolecules is also used in [53]. At \( c_m = 1 \) wt.% (\( \varphi = 0.024 \)), \( T = 296 \text{K} \), pH = 5.0 and \( I = 0.023 \) M the hydrodynamic radius is equal to \( R_D^{(\text{BSA})} = 37.9 \text{Å} \). This value also correlates...
well with that obtained from the analysis of Figure 3, if the corresponding curve is extrapolated to the concentration values of ~1 wt.% (ϕ = 0.024).

In [54], the self-diffusion coefficient for dilute BSA aqueous solutions (c_m = 2.79 wt.% (ϕ = 0.08), T = 298 K, pH = 4.7) was obtained and using equations (17) and (21), one can calculate \( R_D^{(BSA)} = 36.9 \) Å. This value is somewhat less than the value of the hydrodynamic radius \( R_\eta^{(BSA)} = (41.50 \pm 0.05) \) Å obtained from the analysis of viscosity of BSA aqueous solution with properties \( c_m = 2.79 \) wt.% (ϕ = 0.08), T = 298 K, pH = 5.2. Here some discrepancy of values of BSA hydrodynamic radii can be connected with the discrepancy of acid-base balances (pH) of solutions and the presence of ions of salts in solutions.

In [55] on the basis of viscosity data for extremely diluted BSA solutions using the generalized Einstein formula for elongated macromolecules [56] the effective length of the large spheroid axis of the revolution was obtained: \( R_\eta^{(BSA)} = 41.5 \) Å.

A comparison of the values of effective radii of BSA macromolecules calculated from viscosity data according to equation (13) and self-diffusion coefficient according to equation (17) is presented in Table 1. The properties of the solution – temperature T, acid-base balance pH, and concentration of ions in the solution I– are given in brackets.

| \( c_m \), wt.% | ϕ   | \( R_\eta(T, pH, I) \), Å | \( R_\eta(T, pH, I) \), Å |
|--------------|-----|--------------------------|--------------------------|
| 1.00         | 0.024 | 35.6 (296 K; 5.2; 0 M)   | 37.9 (296 K; 5.0; 0.023 M) |
| 2.14         | 0.06  | 39.90 (298 K; 5.2; 0 M)  | 39.92 (298 K; 5.0; 0.15 M) |
| 2.79         | 0.08  | 41.5 (298 K; 5.2; 0 M)   | 36.9 (298 K; 4.7; 0.1 M)  |

* calculation result using corrections due to equations (20)–(21).

Thus, the results obtained by us correlate well with data from other sources. Also, correction of the hydrodynamic radius of albumin macromolecules by equations (20)–(21) allows us to achieve almost complete consistency of data obtained from shear viscosity and self-diffusion. Some ambiguity of macromolecule radii comparison is determined by a mismatch between the pH of a solution and the presence of ions of salts, to which albumin structure is sensitive.

### 3.3. Effective radii of human serum albumin macromolecules

To obtain temperature and concentration dependencies of effective radii of HSA macromolecules we use cell approach equations (13), (14), and (2) and experimental values of shear viscosity in [57]. The surface of effective radii of HSA macromolecules as a function of temperature in the interval (278 \pm 318) K and concentration in the interval (0.82 \pm 18.2) wt.% (ϕ = (0.03 \pm 0.48)) for the value pH = 7.0 is presented in Figure 4.

Work [57] shows that three concentration intervals can be identified over the entire temperature range 1) (0.82 \pm 3.65) wt.% (ϕ = (0.03 \pm 0.14)), where the effective radii of human serum albumin remain unchanged; 2) (4.67 \pm 9.45) wt.% (ϕ = (0.18 \pm 0.31)), where the effective radii of albumin in
aqueous solution decrease and 3) \((10.2 \div 18.2)\) wt.% \((\varphi = (0.33 \div 0.48))\), where the effective radii of albumin macromolecules with increasing concentration linearly decrease, and the slope is poorly dependent on temperature (Figure 5).

**Figure 4.** Temperature and concentration dependence of effective radii of human serum albumin macromolecules at pH value 7.0 [57].

**Figure 5.** Concentration dependence of effective radii of HSA macromolecules along isotherms at pH value 7.0 [57].

In [57] the dependencies of concentration on temperature are constructed, at which the radius of an HSA macromolecule remains unchanged. The curve that corresponds \(R_{\eta}^{(HSA)} = (42.53 \pm 0.05)\text{Å}\) in the concentration interval \((7.0 \div 10.0)\) wt.% \((\varphi = 0.21 \div 0.28)\) has two minimums at temperatures \(T_{\text{min}1} = (298 \pm 1)K\) and \(T_{\text{min}2} = (314 \pm 1)K\), one maximum at temperature \(T_{\text{max}} = (303 \pm 1)K\) (see Figure 6). At the same time, the temperature interval between the local minimums corresponds to the boundaries of warm-blooded organisms [57]. In [58], the change of albumin conformation in the temperature range (293–338) K is associated with the dynamic phase transition occurring in the
water at ~315 K (42 °C). The role of interactions of water with albumin macromolecules increases with the growth of HSA concentration. The authors in [59] attribute the albumin conformation dynamics to changes in water properties occurring in the physiological temperature interval.

Let us compare the sizes of HSA macromolecules obtained from the analysis of the shear viscosity of its aqueous solutions with the available literature data. In [13] using the small-angle neutron scattering some dilute HSA aqueous solutions (I = 0.15 M) were investigated: the results indicate the conformation probability of HSA macromolecule as an asymmetric prolate ellipsoid with a radius of 42.5 Å, which correlates well with our results.

In [59,60] using the photon correlation spectroscopy and molecular dynamics in dilute HSA aqueous solutions (c_m = 0.1 wt.% (φ = 0.004), T=(298 ÷ 323) K, (0.075 < I < 0.225) M) the independence of the value of hydrodynamic radius \( R_D^{(HSA)} = (50 \pm 3) \) Å from temperature is shown, that well correlates with the results for concentrations \( \phi < 0.15 \) obtained by us (see Figure 5). Some discrepancies between our results of \( R_D^{(HSA)} = 44 \) Å macromolecules of HSA and the value of \( R_D^{(HSA)} = (50 \pm 3) \) Å in [59] can be attributed to the presence of sodium chloride ions in the last solutions.

In [9,61] somewhat smaller values of the hydrodynamic radius \( R_D^{(HSA)} = (30.5 \pm 0.5) \) Å obtained by the dynamic light scattering for dilute HSA aqueous solutions (c_m = (0.5 ÷ 2) wt.% (φ = 0.018 ÷ 0.074), T = 298 K, pH = 7.0) are presented. These values of hydrodynamic radii of HSA macromolecules are comparable with the gyration radii of HSA macromolecules, obtained by the small-angle neutron scattering method in [16]. In [9] the independence of the hydrodynamic radius value from the concentration for dilute HSA solutions is observed, which is typical for the temperature-concentration dependence in the interval of dilute HSA solutions obtained by us (φ < 0.15).

The cellular approach (1)–(14) turns out to be a rather simple, efficient method for the determination of the macromolecular radii from the shear viscosity data for the macromolecular solutions. In other hand, the determination of the macromolecular size in the framework of the dynamic light scattering method is a multistage process, each step of which requires the application of certain physical models with their own approximations and errors. An experimental accessibility

**Figure 6.** Temperature dependence of the concentration of the aqueous albumin solutions corresponding to constant radii of macromolecular coils [57].
of the capillary viscometry method and an ability to quickly change the solution composition during the study make it possible to obtain the dependence of the macromolecular size on the temperature, concentration, pH, and ionic composition of the solution, which is important for understanding the complicated dynamics of biomacromolecules in the aqueous solutions.

Thus, the results obtained by us are comparable with the literature sources data. As above, the comparison of macromolecule radii is complicated by the mismatch between pH solution and the presence of salt ions, to which albumin structure is sensitive.

4. Conclusions

The article is devoted to the discussion of changes in the structure and size of PVA, BSA, and HSA macromolecules in aqueous solutions depending on temperature, concentration, and acid-base balance (pH) of the solution. Special attention is paid to the comparison of hydrodynamic radius values obtained from data on self-diffusion of macromolecules and shear viscosity of aqueous macromolecular solutions. The importance of these issues is determined by the necessity of careful consideration of water influence on protein structure.

The determination of macromolecule radii from the shear viscosity of its solutions using cellular approaches proves to be one of the simplest and most effective methods. An important feature of the cell approach used by us [23,24] is that it leads to the results that exactly coincide with those obtained by the Einstein equation [21] and the Batchelor equation [22]. It complements and clarifies the features of macromolecule dynamics in aqueous solutions obtained by other methods.

It should be emphasized that the analysis of macromolecule sizes obtained by different methods is extremely important for investigating changes in the macromolecular coil structure due to their interaction with water at the dissolution in it, as well as considering the interaction between the peripheries of different coils, especially at their overlap, and interaction with ions of acids and alkalis dissolved in water.

References

1. Fenimore PW, Frauenfelder H, Magazù S, et al. (2013) Concepts and problems in protein dynamics. Chem Phys 424: 2–6.
2. Peters JrT (1996) All about Albumin: Biochemistry, Genetics, and Medical Applications, New York: Academic Press, 1–432.
3. He XM, Carter DC (1992) Atomic structure and chemistry of human serum albumin. Nature 358: 209–215.
4. Majorek KA, Porebski PJ, Dayal A, et al. (2012) Structural and immunologic characterization of bovine, horse, and rabbit serum albumins. Mol Immunol 52: 174–182.
5. Akdogan Y, Reichenwallner J, Hinderberger D (2012) Evidence for water-tuned structural differences in proteins: an approach emphasizing variations in local hydrophilicity. PLoS ONE 7: e45681.
6. Carter DC, Ho JX (1994) Structure of serum albumin. Adv Protein Chem 45: 153–203.
7. Pagnotta SE, Ricci MA, Bruni F, et al. (2008) Water structure around trehalose. Chem Phys 345: 159–163.
8. Magazù S, Migliardo F, Benedetto A, et al. (2011) Thermal behavior of hydrated lysozyme in the presence of sucrose and trehalose by EINS. J Non-Cryst Solids 357: 664–670.
9. Luik AI, Naboka YuN, Mogilevich SE, et al. (1998) Study of human serum albumin structure by dynamic light scattering: two types of reactions under different pH and interaction with physiologically active compounds. *Spectrochim Acta A Mol Biomol Spectrosc* 54: 1503–1507.

10. Maslova MN, Zaritskiy AR, Chaykov LL (2014) The blood plasma particles sizes oscillations observed by dynamic light scattering. *Biophys J* 106: 457a–458a.

11. Magazù S, Maisano G, Migliardo P, et al. (1999) Experimental simulation of macromolecules in trehalose aqueous solutions: a photon correlation spectroscopy study. *J Chem Phys* 111: 9086–9092.

12. Sjöberg B, Mortensen K (1994) Interparticle interactions and structure in nonideal solutions of human serum albumin studied by small-angle neutron scattering and Monte Carlo simulation. *Biophys Chemist* 52: 131–138.

13. Kiselev MA, Gryzunov YA, Dobretsov GE, et al. (2001) The size of human serum albumin molecules in solution. *Biophysics* 46: 423–427.

14. Varga B, Migliardo F, Takacs E, et al. (2008) Neutron scattering studies on dUTPase complex in the presence of bioprotectant systems. *Chem Phys* 345: 250–258.

15. Chicea D, Chicea R, Chicea LM (2013) HSA particle size characterization by AFM. *Rom Reports Phys* 65: 178–185.

16. Olivieril JR, Craievich AF (1995) The subdomain structure of human serum albumin in solution under different pH conditions studied by small angle X-ray scattering. *Eur Biophys J* 24: 77–84.

17. Wilkins DK, Grimshaw SB, Receveur V, et al. (1999) Hydrodynamic radii of native and denatured proteins measured by pulse field gradient NMR techniques. *Biochem* 38: 16424–16431.

18. Magazù S (2000) NMR, static and dynamic light and neutron scattering investigations on polymeric aqueous solutions. *J Mol Struct* 523: 47–59.

19. Qian J, Tang Q, Cronin B, et al. (2008) Development of a high performance size exclusion chromatography method to determine the stability of human serum albumin in a lyophilized formulation of Interferon alfa-2b. *J Chromatogr A* 1194: 48–56.

20. Monkos K (2004) On the hydrodynamics and temperature dependence of the solution conformation of human serum albumin from viscometry approach. *BBA-Proteins Proteom* 1700: 27–34.

21. Einstein A (1906) Eine neue bestimmung der moleküldimensionen. *Ann Phys* 19: 289–305.

22. Batchelor GK (1967) *An Introduction to Fluid Dynamics*, Cambridge: Cambridge university press, 1–615.

23. Malomuzh NP, Orlov EV (2005) Static shear viscosity of a bimodal suspension. *Ukr J Phys* 50: 618–622.

24. Orlov EV (2010) Shear viscosity of dispersions of particles with liquid shells. *Colloid J* 72: 820–824.

25. Khorolskyi OV (2018) Effective radii of macromolecules in dilute polyvinyl alcohol solutions. *Ukr J Phys* 63: 144–149.

26. Mooney RCL (1941) An X-ray study of the structure of polyvinyl alcohol. *J Am Chem Soc* 63: 2828–2832.

27. Bunn CW (1948) Crystal structure of polyvinyl alcohol. *Nature* 161: 929–930.

28. Colvin BG (1974) Crystal structure of polyvinyl alcohol. *Nature* 248: 756–759.

29. Gowariker VR, Viswanathan NV, Sreedhar J (1986) *Polymer science*, New York: Wiley, 1–505.
30. Rumyantsev M, Gushchin A, Zelentsov S (2012) Effect of the type of hydrogen bonding on the reactivity of hydroxyl groups in the acetalization of poly(vinyl alcohol) with butanal. Polym Sci Series B 54: 464–471.
31. Karunakaran DJSA, Ganesh T, Sylvester MM, et al. (2014) Dielectric properties and analysis of H-bonded interaction study in complex systems of binary and ternary mixtures of polyvinyl alcohol with water and DMSO. Fluid Phase Equil 382: 300–306.
32. Tamai Y, Tanaka H, Nakanishi K (1996) Molecular dynamics study of polymer-water interaction in hydrogels. 1. Hydrogen-bond structure. Macromolecules 29: 6750–6760.
33. Budhlall BM, Landfeater K, Sudol ED, et al. (2003) Characterization of partially hydrolyzed poly(vinyl alcohol). Effect of poly(vinyl alcohol) molecular architecture on aqueous phase conformation. Macromolecules 36: 9477–9484.
34. Fileti EE, Chaudhuri P, Canuto S (2004) Relative strength of hydrogen bond interaction in alcohol-water complexes. Chem Phys Lett 400: 494–499.
35. Pal S, Kundu TK (2012) Theoretical study of hydrogen bond formation in trimethylene glycol-water complex. Int Scholarly Res Notices 2012: 570394.
36. Rumyantsev M (2013) Influences of co-solvent on hydrogen bond reorganization in ternary poly(vinyl alcohol) solutions. Eur Polym J 49: 2257–2266.
37. Rumyantsev M, Zelentsov SV, Gushchin AV (2013) Retardation effect in acetalization of poly(vinyl alcohol) with butyraldehyde. Eur Polym J 49: 1698–1706.
38. Malomuzh NP, Bulavin LA, Gotsulskyi VYa, et al. (2020) Characteristic changes in the density and shear viscosity of human blood plasma with varying protein concentration. Ukr J Phys 65: 151–156.
39. Rumyantsev M, Rumyantsev S, Kazantsev OA, et al. (2020) Managing of hydrogen bonding in aqueous poly(vinyl alcohol) solutions: new perspectives towards preparation of more homogeneous poly(vinyl butyral). J Polym Res 27: 52.
40. Groda YG, Vikhrenko VS, Poghosyan AH, et al. (2015) Conformation and diffusion properties of polyvinyl alcohol and polyvinylpyrrolidone molecules. Elect J Nat Sci 24: 60–67.
41. Fisenko AI, Malomuzh NP (2009) To what extent is water responsible for the maintenance of the life for warm-blooded organisms? Int J Mol Sci 10: 2383–2411
42. Bulavin LA, Malomuzh NP (2010) Dynamic phase transition in water as the most important factor of provision of denaturation of proteins in heat blood organisms. Phys Alive 18: 16–22.
43. Migliardo F, Magazù S, Caccamo MT (2013) Infrared, raman and INS studies of poly-ethylene oxide oligomers. J Mol Struct 1048: 261–266.
44. Caccamo MT, Magazù S (2016) Tagging the oligomer-to-polymer crossover on EG and PEGs by infrared and raman spectroscopies and by wavelet cross-correlation spectral analysis. Vibr Spectr 85: 222–227.
45. Garvey M, Tadros T, Vincent B (1974) A comparison of the volume occupied by macromolecules in the adsorbed state and in bulk solution: Adsorption of narrow molecular weight fractions of poly(vinyl alcohol) at the polystyrene/water interface. J Colloid Interf Sci 49: 57–68.
46. Wang B, Mukataka S, Kokufuta E, et al. (2000) Viscometric, light scattering, and size exclusion chromatography studies on the structural changes of aqueous poly(vinyl alcohol) induced by γ-ray irradiation. J Polym Sci Pol Phys 38: 214–221.
47. Wiśniewska M (2012) Temperature effects on the adsorption of polyvinyl alcohol on silica. Cent Eur J Chem 10: 1236–1244.
48. Khorolskyi OV, Moskalenko YuD (2020) Calculation of the macromolecular size of bovine serum albumin from the viscosity of its aqueous solutions. Ukr J Phys 65: 41–49.
49. Magazù S, Calabrò E (2011) Studying the electromagnetic-induced changes of the secondary structure of bovine serum albumin and the bioprotective effectiveness of trehalose by Fourier transform infrared spectroscopy. J Phys Chem B 115: 6818–6826.
50. Magazù S, Calabrò E, Campo S, et al. (2012) New insights into bioprotective effectiveness of disaccharides: an FTIR study of human haemoglobin aqueous solutions exposed to static magnetic fields. J Bio Phys 38: 61–74.
51. Minutoli L, Altavilla D, Bitto A, et al. (2008) Trehalose: a biophysics approach to modulate the inflammatory response during endotoxic shock. Eur J Pharm 589: 272–280.
52. Yadav S, Shire SJ, Kalonia DS (2011) Viscosity analysis of high concentration bovine serum albumin aqueous solutions. Pharm Res 28: 1973–1983.
53. Gaigalas AK, Hubbard JB, McCurley M, et al. (1992) Diffusion of bovine serum albumin in aqueous solutions. J Phys Chem 96: 2355–2359.
54. Keller KH, Canales ER, Yum SI (1971) Tracer and mutual diffusion coefficients of proteins. J Phys Chem 75: 379–387.
55. Jachimska B, Pajor A (2017) Physico-chemical characterization of bovine serum albumin in solution and as deposited on surfaces. Bioelectrochem 87: 138–146.
56. Brenner H (1974) Rheology of a dilute suspension of axisymmetric brownian particles. J Multiphase Flow 1: 195–341.
57. Khorolskyi OV (2019) Calculation of the effective macromolecular radii of human serum albumin from the shear viscosity data for its aqueous solutions. Ukr J Phys 64: 287–292.
58. Bardik V, Gotsulskii V, Pavlov E, et al. (2012) Light scattering study of human serum albumin in pre-denaturation: relation to dynamic transition in water at 42 °C. J Mol Liq 176: 60–64.
59. Atamas N, Bardik V, Bannikova A, et al. (2017) The effect of water dynamics on conformation changes of albumin in pre-denaturation state: photon correlation spectroscopy and simulation. J Mol Liq 235: 17–23.
60. Atamas N, Bardik VY, Komisarenko S, et al. (2019) Water dynamics and stability of major blood proteins at pre-denaturation stage. Atti Accad Pelorit Pericol Cl Sci Fis Mat Nat 97: A16.
61. Hushcha TO, Luik AI, Naboka YN (2000) Conformation changes of albumin in its interaction with physiologically active compounds as studied by quasi-elastic light scattering spectroscopy and ultrasonic method. Talanta 53: 29–34.

© 2020 the Author(s), licensee AIMS Press. This is an open access article distributed under the terms of the Creative Commons Attribution License (http://creativecommons.org/licenses/by/4.0)