Methods for Predicting Ethylene/Cyclic Olefin Copolymerization Rates Promoted by Single-Site Metallocene: Kinetics Is the Key

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Abstract: In toluene at 50 °C, the vinyl addition polymerization of 4-vinyl-cyclohexene (VCH) comonomers with ethylene is investigated using symmetrical metallocene (rac-En(Ind)2ZrCl2) combined with borate/TIBA. To demonstrate the polymerizations’ living character, cyclic VCH with linear-exocyclic and endocyclic bonds produces monomodal polymers, but the dispersity (D) was broader. The copolymers obtained can be dissolved in conventional organic solvent and have excellent thermal stability and crystalline temperature (ΔHm), and their melting temperature (Tm) varies from 109 to 126 °C, and ΔHm ranges from 80 to 128 (J/g). Secondly, the distribution of polymeric catalysts engaged in polymer chain synthesis and the nature of the dormant state are two of the most essential yet fundamentally unknown aspects. Comprehensive and exhaustive kinetics of E/VCH have shown numerous different kinetic aspects that are interpreted as manifestations of polymeric catalysts or of the instability of several types of active center [Zr]/[C*] fluctuations and formation rates of chain propagation Rpe, Rp-VCH, and propagation rate constants kpE and kp-VCH, the quantitative relationship between RpE, Rp-VCH and kpE, kp-VCH and catalyst structures, their constituent polymer Mw, and their reactivity response to the endocyclic and exocyclic bonds of VCH. The kinetic parameters RpE, Rp-VCH, kpE, and kp-VCH, which are the apparent rates for the metallocene-catalyzed E/VCH, RpE, and kpE values, are much more significant than Rp-VCH and kp-VCH at 120 s, Rpe and Rp-VCH 39.63 and 0.78, and the kpE and kp-VCH values are 6461 and 93 L/mol·s, respectively, and minor diffusion barriers are recommended in the early stages. Compared with previously reported PE, RpE and kpE values are 34.2 and 7080 L/mol·s. VCH increases theRpE in the initial stage, as we are expecting; this means that the exocyclic bond of VCH is more active at the initial level, and that the chain transfer reaction of cyclic internal π double is increased with the reaction time. The τp versus RpE, kpE, and [Zr]/[C*] fraction count may be fitted to a model that invokes deactivation of growing polymer chains. At τp = 120–360 s higher, the incorporation rate of VCH suppresses E insertion, resulting in reduced molecular weight.

Keywords: metallocene; 4-vinyl-cyclohexene; borate; ethylene; kinetics; polymerization
1. Introduction

Cyclic dienes (e.g., norbornane N.B), dicyclopentadiene (DCPD), 5-ethyldiene-2-norbornene (ENB), 5-vinyl-2-norbornene (VNB), and 4-vinylcyclohexene (VCH) can be prepared by a reaction in multiple fundamentally different ways, relying upon the weather already bound by vinyl addition reactions, radical and cationic polymerization, and ring-opening metathesis olefin polymerization [1–4]. Compared to cyclic dienes synthesized by radical or cationic and ring-opening polymerization, vinyl addition cyclic dienes exhibit excellent thermal stability, low dielectric constant, and higher glass-transition temperature, all of which are a result of the double bond cyclic backbone chain structure [5–7]. Co- and terpolymers of ethylene/propylene (EPM) and ethylene/propylene/diene (EPDM) are significant manufacturing thermoplastics [8–11]. Throughout the last few decades, EPM and EPDM have been suitable choices for synthetic plastic and rubber due to their superior weatherability and mechanical properties. The α-olefin (propylene, cyclic and linear diene)-based polymers play a significant part in people’s daily lives. A substantial amount of rubber, plastics, and fiber materials are manufactured each year using these monomers. According to Worldwide Information, Inc.’s analytics, EPDM global production is growing at a rate of 4% per year and will exceed 1.9 million tons annually by 2023 [10,12–15].

Typical slightly elevated catalysts are based on metallocene or post-metallocene complexes. Remarkably, metallocene catalysts include sandwiches having C\textsubscript{1} [8,9], C\textsubscript{s} [9,10], and C\textsubscript{2} [11,12] symmetries, as well as complexes with restricted geometry [13]. Half-sandwich Ti (IV) complexes containing nitrogen anionic donor ligands such as ketimides, phosphine imides, iminomimidazolidinates, amidinates, and guanidinates are especially promising post-metallocene catalysts for EPDM manufacture [14]. Since the late 1980s, a wide range of single-sight ansa-metallocene polymeric catalysts have made it possible to produce EPM and EPDM with a wide range of composition, an extensive range of physical properties, structural diversity, greater incorporation of numerous cyclic and linear dienes without gel growth, and the production of a higher molecular weight EPM and EPDM with a narrow molecular weight distribution at elevated pressure and temperatures [14,16–18]. The single-site Group IV metallocene catalysts discovered in the late 1950s have received considerable commercial attention. One of the essential characteristics of these catalysts is their open active site, which enables the incorporation of additional olefins or α-olefins into P.E. A number of papers in the literature describe the co- and ter- polymerization of ethylene with linear α-olefins such as hexene and octane, as well as cyclic monomers such as norbornene (N.B., ENB, VNB, and DCPD) and VCH. In addition, recent advances in metallocene-catalyzed chain-shuttling polymerization have helped broaden the spectrum of these already diverse polymeric catalyst systems [19–21]. Similarly, the manufacturing output of P.E., P.P., EPM, and EPDM polymers with conventional Ziegler–Natta polymeric catalysts has decreased relative to polyolefin manufacture utilizing metallocene [17–22].

In post-metallocene and metallocene catalysts, the most efficient cocatalysts are methylaluminoxane and their derivatives methylaluminoxane (MAO) and modified methylaluminoxane (MMAO), which are employed in the commercial synthesis of EPM and EPDM [22–24]. Regardless of the fact that MAO is, in actuality, the facilitator of such systems, its use as an activator has considerable disadvantages. These include high cost, the requirement to employ it in large molar excess to pre-catalysts, and the loss of stability during prolonged storage, resulting in loss of activating capabilities and irreproducibility of polymers properties. According to the literature, triisobutylaluminium (TIBA)/borate is an excellent activator of metallocene complexes in the polymerization of olefins [25–28].

Metallocenes/TIBA/borates and metallocenes/triethylaluminium (TEA)/borates have been exploited as catalysts for both homo-, co-, and ter- polymerizations. While these catalytic systems have demonstrated impressive outcomes in homopolymerization, several complications have arisen when two or more monomers are supplied in the system for polymerization. Depth of knowledge of the kinetics and mechanism of polymeric metallocene canalization α-olefin co/terpolymer process would impressively aid the development of better polymerization process optimizations and an improved metallocene catalyst system.
A kinetic investigation based on active center [Zr][C*] concentration measurements during the polymerization process can offer direct characteristic information on polymeric catalyst activation efficiency and the nature of the active sites, which are crucial for illustrating the catalysis mechanism. There are only a few publications in the literature on the kinetics and mechanism of metallocene-catalyzed olefin co- and ter- polymerization based on active center counts. Furthermore, the contributions of R. Landis [25], Chen [4], Fan [22], Kaminsky [26], Bochmann [27], and M. Waymouth [5] have resulted in significant progress in the establishment of innovative copolymerization metallocene catalysts.

Unfortunately, few catalysts have been defined in terms of kinetics, partly because of the lack of procedures for required important information, such as active site [Zr][C*] counts. Although the kinetics of a wide range of catalysts have yet to be determined, the fundamental aspects of catalytic olefin polymerization are well understood [19–21]. There are multiple steps in rac-Me2Si(2-Me-4-Ph-Ind)2ZrCl2/[Ph3C][B(C6F5)4], racEt(Ind)2ZrCl2/[Ph3C][B(C6F5)4]-catalyzed olefin polymerization: initiation into a metal alkyl (M-R) bond, propagation through the resulting inserts, and chain transfer following either 2,1 or 1,2-α-olefin inserts. This has been demonstrated in previous studies [26,29]. Catalyst inactivity or dormancy, death, and other improbable outcomes are possible extra phases [7,25]. It is currently difficult for researchers to quickly determine the kinetics of polymerization for many different catalysts. Finding new and better ways to count active sites has historically contributed significantly to the field’s core knowledge and technological advancements [21,30].

The present study’s major objective is to examine the kinetic behavior of ethylene and 4-vinyl cyclohexene (VCH) with symmetrical rac-Et(Ind)2ZrCl2/activated by triisobutylaluminum/ [Ph3C][B(C6F5)4] cocatalysts in gaseous phase reactors to use a model with parameters determined from gas- and slurry-phase rac-Et(Ind)2ZrCl2/MMAO. The number of active centers (C/[Zr]) in different copolymerization runs was measured using the quench-labeling technique utilizing (TPPC) as a quenching agent to better understand the process of E/P copolymerization with metallocene/borate catalysts. In order to better understand the mechanism of E/VCH with the above catalyst system, by quench-labeling polymer propagation chains in the system using thiophene-2-carbonyl chloride as the quenching agent, the practical approach adopted in the study was an experimental assessment of active center fraction (molar ratio of metallocene and active centers in the system). The propagation rate constant, RpE, and RpVCH, the kinetic rate constant of chain propagation (kpe and kpVCH), were determined based on the data of polymerization activity and equilibrium of ethylene. Furthermore, we explored the connection between catalyst arrangement, polymer morphology, and microstructure in E/VCH copolymerization. It will be possible to learn more about the mechanism of single-site metallocene-catalyzed ethylene with α-olefins copolymerization by studying the kinetics of E/VCH, particularly the association between the catalytic active-site properties and the structure of the polymeric catalyst. It has been reported in our previous study that the active centers in rac-Et(Ind)2ZrCl2/MMAO and rac-Et(Ind)2ZrCl2/triisobutylaluminum/[Ph3C][B(C6F5)4]-catalyzed E/P copolymers grew steadily at first, but eventually reached an all-time high of 98.7%, which was significantly higher than the maximum value of polyethylene [11,25,31]. It will be much more encouraging to examine how the activation efficiency and dynamic as well as kinetic features of rac-Et(Ind)2ZrCl2/trisobutylaluminum/[Ph3C][B(C6F5)4] are affected by the replacement of propylene with cyclic diene and their endocyclic double bond effect on the propagation rate constant, RpE, and RpVCH, kinetic rate constant of chain propagation (kpe and kpVCH). However, active site counts (or the proportion of active catalyst) must be measured over time to establish precise polymerization kinetics.

2. Polymerization

All E/VCH polymerizations were carried out in a 100 mL Schlenk flask with a rounded bottom. Before beginning polymerization, the reactor was heated up to 100 °C under vacuum for 45 min and then backfilled with nitrogen gas. The Schlenk flask reactor was filled with the required volume of toluene and then saturated with 0.1 MPa ethylene at
50 °C. After injecting VCH (0.06 mol/L) into the reactor, adding TIBA (2 M) running it for 5 min, and followed by a suitable quantity of zirconocene, the catalyst and borate in toluene solutions were added. During copolymerization, 0.1 MPa E was continuously fed into the reactor. TPPC (TPCC/Al = 2) was injected five minutes after the intended time. The unreacted TPCC and TIBA decomposed with dehydrated ethanol containing 2% hydrochloric acid. This was followed by filtering of the precipitated polymers, several washes with 95% ethanol, and subsequently drying in a vacuum at room temperature to constant weight [25,26,32].

3. Materials

Handling moisture and air-sensitive materials were accomplished in an inert glove box. Zhejiang Mixing Gas Co. (Hangzhou, China) supplied the ethylene and further refined it with a gas purification column and molecular sieves. By flushing the gases, oxygen was removed. Comonomer 4-vinyl-cyclohexene (VCH) was obtained from Aldrich and dehydrated by stirring it for 6 h over CaH₂. It was then refined further by dehydrating it through 4 Å molecular sieves, distilling it under reduced pressure, and storing it in an N₂ gas atmosphere. Sigma-Aldrich supplied the symmetrical ansa-metallocene (rac-Et(Ind)₂ZrCl₂). Albemarle Co. Shanghai, China, provided the cocatalyst trisobutylaluminum (TIBA), and the borate (Ph₃C)B(C₆F₅)₄ activator was prepared according to the published literature. J&K Scientific, PR China, supplied the quenching agent TPCC with 98% purity. Toluene reaction solvent (Aldrich, 99.7%) was refluxed for 4 h over sodium benzophenone, distilled, and stored on molecular sieves under nitrogen. The TPCC was distilled first, then diluted to 2.0 M with distilled n-heptane before use.

4. Characterizations

An ultra-violet fluorescence sulfur detector, the YHTS-2000, was utilized to measure the sulfur (S) content of each E/VCH polymer sample and take the average value content from pure E/VCH synthetic polymer parallel samples. Each sample was assessed for sulfur (S) content three times, and the mean values were used to calculate the S percentage.

In making the comparison with the quench-labeled pure samples, which already had S concentrations ranging from 5 to 20 ppm, the S content in a blank E/VCH sample produced under typical conditions but without the quenching step was approximately 0 ppm (see Scheme 1) [29,33]. A mechanistic model was proposed to explain the observed phenomena in detail. E and VCH copolymerization create non-active sites, and the VCH endocyclic double bonds become chelated with Zr metal and interact with the catalyst ligand. Thus, the latter portion of this study explains how VCH activates the inactive site.

The resulting copolymers ¹H NMR were obtained using a Varian Mercury plus 300 spectrometers in pulse Fourier transform type functioning at 75 MHz. The experiments were carried out in o-dichlorobenzene-d₄ with a copolymer solution containing 10% by weight and hexamethyldisiloxane as an internal reference at 120 °C. Cr (acac)₃ was introduced to moderate the relaxation duration of carbon atoms, and the pulse delay time was set to 3 s [31,34]. The pulse was angled at 90°. It took 0.8 s to complete the acquisition. The spectral width was 8000 Hz, and inverse gated decoupling was utilized for integration. On average, around 4000 scans were collected. Previous research confirmed the ¹H NMR peak assignment [34]. The ¹H NMR spectra of copolymer samples are shown in Supporting information Figure S2. ¹H NMR was used to calculate the amount of inserted comonomers in the copolymers and the comonomer conversion according to the literature [35–37].
Differential scanning calorimetry (DSC) analysis was carried out using TA Q200 equipment calibrated with indium and water. The sample, typically 3–5 mg, was employed in a sealed aluminum pan. To eliminate thermal behavior, the taster was heated to 150 °C for 5 min before being cooled at a rate of 10 °C/min to 20 °C. Lastly, the melting curve was obtained by gradually heating the sample to 180 °C at a rate of 10 °C/min [5,38].

The molecular weight (Mw) and molecular weight distribution (Mw/Mn) of E/VCH copolymers were determined using a high-temperature gel permeation-chromatography PL 220 GPC apparatus with three PL-gel 10 m MIXED-B columns and 1,2,4-trichlorobenzene as the eluent at a flow rate of 1.0 mL/min at a temperature of 150 °C. It was planned for conducting universal calibration against thin polystyrene standards.

5. Result and Discussion

Metallocene catalysts combined with MAO, MMAO, and TIBA cocatalyst have recently been shown to be useful polymeric catalysts in the homopolymerization of ethylene and their co-/ter- polymerization with α-olefins and cyclic olefins [29,31]. The co- and ter-polymerization of E with P and bicyclic (N.B., ENB, and VNB) olefins have been investigated using certainly known metallocene catalysts in the literature [9,12]. However, one of the recommended cyclic dienes, VCH, possesses both linear-exocyclicπ bonds and endocyclicπ bonds, but they differ in terms of reactivity. Under identical experimental conditions, VCH
exhibits exclusive steric hindrance and reactivity, resulting in various copolymerization characteristics. We projected that TIBA (800 Equiv. to Zr) would successfully activate this isospecific rac-Me2Et(Ind)2ZrCl2 catalysts in the presence of borate (2 Equiv. to Zr), which serves as an activator. In addition, TIBA was allowed to react in toluene at 50 °C for 10 min with catalyst precursor and diene impurities. The ethylene (99.9% pure) gaseous monomer was refilled during the reaction time progress by keeping a constant gas pressure (0.1 MPa). At the same time, the liquid VCH comonomers were introduced in the reactor at the start. Under the parameters used, no copolymerization of E with VCH was reported before. However, Table 1 summarizes the typical results of E/VCH copolymerizations. By increasing the polymerization time (t_p) with a fixed feed ratio of 0.06 mol/L VCH with ethylene copolymers, up to 3% may be generated. E/VCH copolymers with a low VCH content were completely insoluble in toluene at 50 °C, indicating that they were not gel-free. Copolymers containing 2–3% VCH were anticipated to be soluble in 1,2,4-trichlorobenzene at 130 °C. Swaminathan Sivaram et al., and Fan et al., found that when the comonomer concentration of the feed increased, the catalytic activity and copolymer intrinsic viscosity was reduced [39]. Following a quick examination of the reaction conditions, it was determined that the most effective results were achieved at 50 °C and an Al/Zr ratio of 800. Earlier research exposed that the catalyst rac-Me2Et(Ind)2ZrCl2 with ethylene bridges had the highest ethylene homo- and E/P copolymerization activity [7,25,29]. TIBA immediately activated the rac-Me2Et(Ind)2ZrCl2/borate and the copolymerization occurred at considerable rates, providing strong ethylene/VCH copolymerization activity in the beginning. Interestingly, increasing ethylene/VCH copolymerization’s reaction time resulted in significantly reduced catalytic activity under identical parameters. As a result, we selected the quenched labeling approach to investigate how bicyclic olefins (VCH) with either an endocyclic π or an exocyclic linear π bond affect metallocene catalytic activity (Figure 1).

### Table 1. Ethylene/vinyl-cyclohexene (E/VCH) copolymerizations.

| RUN | Time | Yield | VCH in Pol | Activity | *C | Mw | PD | Tm | ∆Hm |
|-----|------|-------|------------|----------|----|----|----|----|-----|
| 1.1 | 120  | 0.29  | 1.43       | 0.69     | 14.72 | 48,785 | 3.34 | 109.6 | 96.28 |
| 1.2 | 240  | 0.57  | 1.56       | 0.68     | 25.68 | 59,543 | 4.07 | 117.56 | 115.05 |
| 1.3 | 360  | 0.66  | 1.65       | 0.52     | 37.89 | 63,549 | 4.23 | 117.59 | 116.4 |
| 1.4 | 480  | 0.69  | 1.53       | 0.41     | 49.16 | 68,785 | 4.41 | 115.52 | 103.0 |
| 1.5 | 840  | 1.20  | 1.46       | 0.41     | 61.27 | 76,888 | 4.68 | 117.25 | 83.98 |
| 1.6 | 1200 | 1.42  | 1.41       | 0.34     | 66.17 | 82,693 | 4.77 | 114.84 | 90.38 |
| 1.7 | 1500 | 1.69  | 1.35       | 0.32     | 69.58 | 87,301 | 4.99 | 115.07 | 77.94 |
| 1.8 | 1800 | 1.82  | 1.22       | 0.29     | 73.38 | 91,652 | 4.91 | 126.00 | 128.01 |

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Table 1 and Figure 1 found that E homo- and E/VCH copolymerization showed higher average activity in the 1800 s. However, the time-dependent variation in the chain propagation rate (R_p) was calculated by differentiating the polymer yield against the time curve (Supporting information, Figures S3 and S4). The [(C*)/[Zr]] of pure polymer samples was

The impact of cyclic and bicyclic olefins exhibiting linear-endocyclic (C*) and endocyclic (C*) bonds on homogeneous metallocene catalysts with a MAO, MMAO catalyst system, including a metalloocene/TIBA/borate system, has not been well explored. It has long been known that raising the quantity of cyclic and linear dienes in the feed, as predicted, reduces the polymerization catalyst activities, but results in higher levels than ethylene homo- and lower levels than ethylene/proplylene copolymerizations. It has been shown that the activity of E/VCH copolymers decreased from the early to late-1800 s. In contrast, the active center [(C*)/[Zr]] fraction was more significant than ethylene homopolymerization but lower than their copolymerization with propylene, and grew dramatically in the early 1000 s. Table 1 and Figure 1 found that E homo- and E/VCH copolymerization showed higher average activity in the 1800 s. However, the time-dependent variation in the chain propagation rate (R_p) was calculated by differentiating the polymer yield against the time curve (Supporting information, Figures S3 and S4). The [(C*)/[Zr]] of pure polymer samples was
calculated using the equation $[S] = [C^*]$ and the reaction time (Supporting information, Tables S1 and S2).

![Figure 1](image.png)

**Figure 1.** Impact of cyclic olefin exhibiting a linear-exocyclic $\pi$ and endocyclic $\pi$ bonds on metallocene catalyst activity and compared with previously reported PE [25].

The rate equation $R_p = k_p [C^*][M]$ ($[M] = 0.085$ mol/L) was used to calculate the time-dependent change of $k_p$. Tables 1 and 2 summarize the results of E/VCH, including time-dependent active center fraction $[C^*]/[Zr]$, $R_p$, $k_p$, $M_w$, $M_W$, and thermal characteristics ($T_m$, $\Delta H_m$). In contrast, Figure 2 shows active center fraction variation with time and polymerization propagation rates.

### Table 2. Ethylene/vinyl-cyclohexene (E/VCH) copolymerizations with kinetic data.

| RUN | Time | VCH | $^\circ C$ | $R_p$ VCH | $R_p$ E | $k_p$ E | $k_p$ VCH |
|-----|------|-----|-----------|-----------|--------|--------|-----------|
|     | See  | In Polymer | %         | molVCH/molcat s | mole/molcat s | L/mol s | L/mol s |
| 1.1 | 120  | 0.29 | 14.72     | 0.78       | 39.63  | 6410   | 93       |
| 1.2 | 240  | 0.57 | 25.68     | 0.66       | 36.72  | 3405   | 48       |
| 1.3 | 360  | 0.66 | 37.89     | 0.55       | 33.94  | 2133   | 28       |
| 1.4 | 480  | 0.69 | 49.16     | 0.46       | 31.41  | 1521   | 18.1     |
| 1.5 | 840  | 1.20 | 61.27     | 0.27       | 24.86  | 966    | 9.18     |
| 1.6 | 1200 | 1.42 | 66.17     | 0.16       | 19.67  | 708    | 5.228    |
| 1.7 | 1500 | 1.69 | 69.58     | 0.1        | 16.17  | 553    | 3.244    |
| 1.8 | 1800 | 1.82 | 73.38     | 0.069      | 13.32  | 432    | 2.1048   |

* Reaction conditions: Solvent toluene = 50 mL, $E = 0.1$ MPa, $VCH = 0.06$ mol/L, activator TIBA 1000 µmol, Borate $(Ph_3C)(C_6F_5)_2 \ 2.50$ µmol, catalyst $(Et(Ind))ZrCl_2 \ 1.25$ µmol and TPCC 2000 µmole. * $^\circ C$ Determined through the sulfur analyzer (see Supporting files). * $R_p$ VCH and $R_p$ E in unit of mmol poly/molcat s. * $k_p$ Propagation constant of VCH and E.
Table 2 Summary of the E/VCH copolymerization observations, including the time-dependent \([\text{C}^*/[\text{Zr}]]\) ratio and kinetic data such as \(R_p^{\text{E}}\), \(R_p^{\text{VCH}}\), \(k_p^{\text{E}}\), and \(k_p^{\text{VCH}}\). Both \(k_p^{\text{E}}\) and \(k_p^{\text{VCH}}\) values dropped considerably with \(t_p\), as shown in Figures 7 and 8, respectively.

However, as shown in Figure 3, the initial polymerization rate of E/VCH copolymerization was even slightly higher than that of E homopolymerization but lower than that of E/P copolymerization, but later ethylene homo and E/VCH showed a more stable rate than E/P copolymerization when the reaction duration was prolonged to 1800 s. It is worth noting that both polymerization systems with the same catalyst showed a high initial polymerization rate, which can be taken as evidence for the rapid initiation of the active centers.

Figure 2. Metallocene catalysts E/VCH copolymers active center [Zr]/[C∗] fraction variation and propagation rates with polymerization time.
Figure 3. Plots of observed propagation rate $R_p$ of VCH copolymerization and compared with reported ethylene homo- and copolymerization with propylene under the same reaction parameters [25,26].

At $50^\circ$C, the E/VCH polymerization activity level decreased in the reaction period of 120 s to 1800 s, and the active center fraction $[\text{Zr}]/[^{*}\text{C}]$ considerably increased in the initial 840 s and subsequently tended toward a steady state of 73%. Figure 2 is comparable to P.E. but lower than their E/P copolymerizations [26]. The decrease in E solubility in toluene at higher temperatures allows for greater VCH incorporations, as investigated by M. Marques and J. C. W. Chien et al. [34,40,41]. However, a significant decrease in VCH insertion is seen compared to E/NBE and E/ENB copolymerization [34,36,42]. Nevertheless, polymerization activity and molecular weight of obtained E/VCH copolymers were comparable with E/NBE and E/P/ENB copolymers. Nevertheless, propagation rate, yield, and Mw of E/NBE and E/P/ENB were much higher than E/VCH copolymers under similar conditions. In E/VCH copolymerization, VCH tends to suppress the ethylene incorporation rate, especially during 120 s to 360 s, and to lower the copolymers’ molecular weight. Comparable findings were observed in earlier investigations [34,43–45]. Additionally, the VCH endocyclic $\pi$ bond may interact with the active species distantly, resulting in a smaller incorporating gap and quicker chain transfer. According to these conclusions, small changes in the architectures of comonomers and catalysts can alter polymer behavior and activity. Furthermore, active sites accumulating on catalyst surfaces account for the rapid growth in inactive sites at the introduction stage. As a result, the cocatalyst and arriving monomer may readily access these active sites, activate before contact, and begin quickly. We investigated the polyethylene chain propagation rate $R_p$ in an earlier study under identical polymerization conditions. We compared it to the E/VCH polymerization rate, finding that P.E. had a significantly higher $R_p$ at first but that the E/VCH copolymerization $R_p$ was more stable when the reaction time was extended to the 1800 s (see Figure 2). It suggests that both polymerization systems demonstrated more excellent early polymerization rates, indicating faster active center activation.
The molecular weight (Mw) of the E/VCH copolymers was lower at the beginning of the reaction but gradually rose with reaction time (t_p). A narrow molecular weight distribution (MWD) of E/VCH copolymers suggests numerous active [Zr]/[C^*] sites in the catalytic system, as the MWD was presumably more than 2 (Supporting information, Figure S1). The chain transfer of the active centers with TIBA could have been responsible. Under comparable polymerization conditions, the rac-Me2Et(Ind)2ZrCl2 metallocene combined with MMAO produced higher molecular weight than the borate cocatalyst system but analogous MWD to the rac-Me2Et(Ind)2ZrCl2/MMAO catalyst. For the rac-Me2Et(Ind)2ZrCl2/borate system, chain transfer of the active centers with TIBA could have been responsible.

Depending on the content of dienes, the E/dienes copolymers were amorphous or had a Tm of 100–120 °C. The thermal properties of E/VCH copolymers with polymerization time are presented in Table 1. Generally, cyclic olefins are bulkier than ethylene and α-olefins and inhibit the rotational movement of polymer, cyclic olefin structure, and concentration; polymerization reaction time also substantially influences the thermal properties (crystalline temperature (ΔH_m) and melting temperature (Tm)). The Tm varies from 101 to 121 °C, but the ΔHm varies from 9 to 16 (J/g). These results are strongly connected to the copolymer composition, indicating that composition drift may have an unexpectedly detrimental influence on thermal properties. VCH-rich segments and chains early in the process might suggest amorphous and crystalline segments with different ethylene sequences, such as higher VCH chain segments that melt at lower temperatures and lower comonomer blocks that melt at higher temperatures.

The E/VCH copolymers 1HNMR (Figure 4) revealed a distinct vinyl pattern between the 4.7 and 6.0 ppm endocyclic C\_1\_ bond and the absence of a strong triplet at the 6.1 ppm linear-exocyclic C\_1\_ bond. The selectivity of copolymerization by enchainment of the endocyclic C\_1\_ bond was determined by 1H NMR using an optimal physical combination of E/VNB copolymers comprising a bicyclic olefin with either an endocyclic or a linear-exocyclic C\_1\_ bond. 1HNMR was also utilized to determine comonomer content (Figure S2). In addition, Figure 5 shows the VCH mol% graph in the E/VCH copolymers vs. the [Zr]/[C^*] ratio in the system.

As we explored, the crystalline appearances of the E/VCH copolymer are lower, and the initial (120–360 s) polymerization rates (k_pE and k_pVCH) are higher due to the more significant insertion VCH in the growing polymer chain; the k_p reaction rates remain constant with decreasing VCH mol%. As shown in Figure 6, the VCH mol% and k_pE and k_p in the E/VCH copolymers are dropped as the reaction time increases from 360 s. This means that the chain termination reaction in E/VCH is faster at the later stage than the initial stage.

The results are analogous to those found in homo- and copolymerization systems of E and α-olefin. In the E/VCH copolymers, k_pE values are noticeably more significant in both stages. At t_p 120 s, the k_pVCH and k_pE are 93 and 6410 L/mol·s, correspondingly, in k_p VCH the beginning stages, the slighter diffusion barriers near the real propagation rate constant were proposed. However, the drop in k_p, as shown in Figures 6 and 7, may be due to a diffusion barrier, as the rate of E diffusion from the bulk of the solution to the [C^*]/[Zr] decreases rapidly when the primary consignment of polymer chains form and consolidate around the [C^*]/[Zr]. Though the [C^*]/[Zr] ratio was enhanced upwards of 2–3 times in the first 480 s, the potential reactivity difference among active centers activated at various phases of the reaction may also produce a substantial variation in the propagation rate constant values. For example, suppose the active catalyst site which is engaged during the 480–840 s period is 40% less active than those catalysts activated during the 120 s, and the former account for approximately 60% of all active centers. In that case, the average propagation rate constant value at 240 s polymerization time will be just 73% at 120 s polymerization time, suggesting no diffusion barrier in the system. In a previous study, we investigated the polyethylene and polypropylene homo- and ethylene/propylene copolymerization propagation rate constant under identical polymerization conditions.
and compared it to the E/VCH propagation rate constant; at 120 s, the $k_{pE}$, $k_{pPP}$, $k_{pPE}$, $k_{pP}$, and $k_{pVCH}$ values are 4170, 250, 176, 21.53, 4266, 6410 and 93.6 L/mol·s, respectively [26,29,31], and the recommended moderate diffusion barriers are close to the real propagation rate constant in the early stages (Figure 8). In addition, the initial $k_{pE}$ and $k_{pPE}$ values of E homo- and E/VCH copolymerization are slightly different (4170 and 6410). Because the initial $[C^*]/[Zr]$ fraction of ethylene-VCH copolymerization is higher than that of ethylene homo-polymerization, and it is recommended that the active centers in these two system be of a different nature [18,25]. In contrast, the active center fraction value of E/P copolymerization is higher than E/VCH copolymerization, and the $k_{pPE}$ value of ethylene/propylene copolymerization is lower than E/VCH copolymerization, which means that these two copolymerization systems have different types of active centers. For example, in the ethylene homo- and E/VCH copolymerization, active centers may be loosely connected ion pairs with large $k_{pE}$ values. In contrast, active centers in the ethylene/propylene copolymerization active centers may be tightly linked ion pairs with low $k_{pE}$.

**Figure 4.** $^1$HNMR (75 MHz) spectra of E/VCH copolymers, $^1$HNMR spectra of purified polymer taken in CDCl$_3$ solvent, 0.5–2 ppm illustrating ethylene region and distinct vinyl pattern is represented in the range of 4.7–6.0 ppm.
Figure 5. Graphical representation of the variation in active centers in E/VCH copolymers as a function of time in toluene solution at 50 °C and compared with ethylene homo-polymerization [25,26].

Figure 6. The change of propagation rate ($R_p$) and VCH mol % in the E/VCH copolymers with increasing polymerization time.
Figure 7. In the E/VCH copolymers, propagation rate constant $k_pE$ values are noticeably greater than $k_pVCH$ in both (earlier and later polymerization time) stages.

To make comparisons between the propagation rate constant and polymer reaction time curves of polyethylene, ethylene/propylene, and ethylene/VCH copolymerization is more understandable; the $k_p$ versus polymer reaction time curves are shown in the comparable graph (Figure 9). The preliminary values obtained for the $k_p$ of ethylene/propylene copolymers are lower than those of the E/VCH copolymers because the E/P copolymers with a higher ratio of propylene (<20 mol%) remain nearly amorphous and may be liquefied in toluene, whereas E/VCH copolymers with lower VCH (mol 2%) are crystalline; this difference may be attributed to a more significant diffusion barrier in the E/VCH copolymer. The propagation rate constant of active centers developed initially in the E/VCH copolymer process tends to be greater than those formed later [25].
Figure 8. Plots of observed propagation rate ($R_p$) and propagation rate constant ($k_p$) in E/VCH copolymers in toluene at 50 °C, with $R_p$VCH and $k_p$VCH representing VCH propagation rate and propagation rate constant, and $R_p$E and $k_p$E representing ethylene kinetic data.

Previously reported E and P homo- and copolymerization with E/VCH copolymerization make the results more fascinating. It is well recognized that propylene is sterically larger than ethylene; a component of the homogeneous-metallocene precursor in the form of contact ion pairs might be incapable of promoting the propylene monomer for further coordination and might lead to its behavior as dormant or inactive in the homopolymerization system. Consequently, polypropylene’s [C*/Zr] ratio will be lower than polyethylene. In contrast, E/P copolymerization demonstrated a higher active center fraction than their homopolymers. This suggests that polypropylene can also reactivate the active sites that have been inactive during ethylene homopolymerization. Similarly, the active center fraction of E/VCH copolymers is higher than ethylene homo and lower ethylene/propylene co-polymers. This means that sterically VCH and other bicyclic dienes such as ENB and its derivatives activate the active site in the metallocene precursor that was inactive in the homopolymerization of E, but that the active site activation efficiency of VCH is less than $\alpha$-olefins and ENB. Even though the cyclic olefins (VCH) have a less sterically linear-exocyclic$_\pi$ bond and endocyclic$_\pi$ bond, it is more difficult to synthesize than $\alpha$-olefins such as propylene or 1-Hexen.
Figure 9. Plots of observed propagation rate ($R_p$), propagation rate constant ($k_p$), and active centers $[\text{C}^*/[\text{Zr}]$ as functions of time in E/VCH copolymers in toluene at 50 °C and their comparisons with kinetic data of polyethylene and ethylene propylene copolymers under similar reaction conditions.

Despite the fact that the VCH is a sterically endocyclic π bond, the complexes collapse or become weaker, and the inserting barriers are greater than that for P additions into the Zr–C. Finally, the introduction of VCH into the system led to a significant drop in inactivity. In addition, there is a steric influence on the VCH insertion due to the VCH endocyclic π bond repulsion with the precatalyst ligand. In addition, endocyclic π bond interaction with the precatalyst Zr metal is also possible (F). Furthermore, the lower active center $[\text{C}^*/[\text{Zr}]$ percentage value of E/VCH copolymers than previously has been reported for ethylene/propylene copolymerization in both the early and stable stages can be related to a greater fraction of ZrCH$_2$CH$_3$-type dormant or inactive site in the former. Evidence supporting the existence of such dormant or inactive sites has been given in the literature [25,46,47]. As seen in Scheme 2, ethylene-induced ZrCH$_2$CH$_3$ species produced in Zr-H can enter an inactive or dormant state through β-agostic contact with a Zr metal center and methyl hydrogen. As the electron deficit of the Zr center grows, the intensity of the β-agostic interaction increases as a function of time. By adding electron-donating
substituents (such as phenyl and methyl etc.) on the catalytic ligand, the Zr center should have a reduced degree of electron deficiency and subsequently a lower proportion of inactive sites [38]. In the suggested mechanistic model (Scheme 2), the catalytic precursor’s active sites with an ethylene/VCH propagating chain (A) may undergo $\beta$-H migration, leading to the construction of Cp2Zr–H species (B), which could then be converted to Cp2Zr–CH$_2$–CH$_3$ (C) by introducing ethylene into the Cp2Zr–H bond. Kissin Y.V. and his colleagues observed that they clarified the comonomer activation impact in the E with P and $\alpha$-olefin polymer reactions employing commercialized heterogeneous synthetic polymeric Z–N catalysts in their model [1,11,14–16]. However, (C) has the ability to revert to a latent state and it is active for E and higher in the $\alpha$-olefin polymer reaction. (D) Occurs as a result of strong $\beta$-agnostic interactions between hydrogen on methyl and Zr metal.

Scheme 2. The proposed explanation is based on a mechanistic concept: how non-active sites are developed during the copolymerization of E and VCH, how the VCH endocyclic $\pi$ bonds are chelated with Zr metal and interact with the catalyst ligand, and therefore how VCH gets activated the inactive site.

The presence of a greater proportion of these inactive or dormant sites in the E/VCH copolymerization is the primary cause for a smaller fraction of active caters in the copolymerization than in previously reported ethylene/propylene copolymerization investigations. It has been noted that the insertion of the VCH linear-exocyclic $\pi$ bond into the hydrogen–zirconium (H–Zr) bond during the E/VCH copolymerization can bypass the polymerization reaction, resulting in an increase in the active center fraction, which is higher than that of their homopolymerization counterparts. However, the VCH bypass
polymerization reaction is slower than E/P, and subsequently results in a decrease in the active center fraction in VCH compared to E/P copolymers [29,46,48].

In the case of ethylene with cyclic diolefins copolymerization catalyzed by metalloocene catalyst, the effect of cyclic olefin (VCH) on metalloocene is very different, as explained in the discussion above. According to the investigation in the literature, ENB and VNB belong to the same class, and their effect was different on polymeric catalysts. Compared to ENB, VCH does not exhibit an electron-donating group at the linear-exocyclic bond that increases the electron deficiency of the edocyclic bond and shows the weakest activation effect on homogeneous metalloocene catalysts for ethylene polymerization [31,34]. In addition, in the case of a low steric effect of the catalyst, the edocyclic bond of the VCH chelate with a catalyst metal atom leads to a strong deactivation effect and a lower active center fraction in the system (G).

In addition, VCH (CH=CH–) insertion in the H–Zr bond can bypass the reactions in the initial stage more rapidly, decrease the dormant sites, and increase the active center fraction in the E/VCH copolymer system through Cp2Zr–(CH=CH–) (E). Peaks of edocyclic bonds in the constructed polymer chain verified the above discussion (Figure S2). However, the formation of active species (C) for the polymerization reaction and dormant or inactive sites (D) may need appropriate adjustments of zirconium metal and alkyl (Zr–iPr) moiety, which required sufficient space between the cation and anion. It is reasonable to believe that the [Cp2Zr-iPr] Cl-borate species with connected contact ion pairs is less likely to enter the inactive state than loosely linked ion pairs. It makes sense that the [Cp2Zr-iPr] Cl-borate species with loosely linked ion pairs is more easily transported into the dormant state than those with contact ion pairs. This assumption is confirmed by a significant increase in the [C*]/[Zr] ratio during the first 120–360 s of E/VCH copolymerizations (Table 1). As seen in Figures 4 and 5, the incorporating rate of VCH is greater during the early polymerization period, and the [C*]/[Zr] approaches 35% and increases to 73% as the polymerization time increases. This suggests that catalytic species generated in the first 120–360 s with loosely connected ion pairs can insert more VCH than catalytic species activated later with contact ion pairs. In addition, loosely connected ion pairs supersede the active ethylene site to a great extent than contact ion pairs, with the result that molecular weight in the initial stage of the polymerization is lower than in the later stage. When all the results mentioned above are compared with previous reports, the E/NBE, E/VNB, and E/ENB copolymers, the E/VCH copolymer reaction with VCH comonomer, Mw, R_E, R_VCH, and the comonomer incorporation rate were significantly less than those of the E/NBE and E/ENB and E/VNB copolymers. This might be attributed to VCH special endocyclic bond. The endocyclic double bond in VCH may be able to engage with the active species remotely, leading to a smaller incorporation zone and a faster chain transfer process [34,35,46]. These findings suggest that minor differences in catalysts and comonomer topologies can influence polymerization behavior.

6. Conclusions

Symmetrical metalloocene catalysts are useful polymeric catalysts for ethylene with α-olefin and cyclic olefin polymerizations. The copolymerization of E with vinyl addition polymerization of 4-vinyl-cyclohexene (VCH) was investigated using symmetrical rac-Et(Ind)2ZrCl2 combined with certain known borate/TIBA cocatalyst systems. To demonstrate the polymerizations’ living character, cyclic VCH with linear-exocyclic and endocyclic bonds produces polymers with a monomodal and narrow molecular weight distribution (MWD) regulated by reaction time. Secondly, the distribution of polymeric catalysts engaged in polymer chain synthesis and the nature of the dormant state are two of the most essential yet fundamentally unknown aspects. Precise research into the Ziegler–Natta polymeric catalyst has demonstrated that a comprehensive kinetic study based on acyl chloride selectively quenched the (Zr, Ti) metal–polymeric bond for assessing olefinic catalysts in the concepts of k_p, R_p, and [Zr]/[°C] ratio, and can be used to evaluate olefinic catalysts. The kinetic parameters R_pE, R_pVCH, k_pE, and k_pVCH, which are the
apparent rates for metallocene-catalyzed E/VCH, $R_p$E, and $k_p$E values, are much more significant than $R_p$VCH and $k_p$VCH at 120 s, $R_p$E and $R_p$VCH 39.63 and 0.78, and the $k_p$E and $k_p$VCH values are 6461 and 93 L/mol·s, respectively, and minor diffusion barriers are recommended in the early stages. When compared with P.E., VCH increases the $R_p$E in the initial stage, which means that the exocyclic bond of VCH is more active at the initial level, and that the chain transfer reaction of cyclic internal π double is increased with the reaction time. The $t_p$ versus $R_p$, $k_p$, and [Zr]/[C*] fraction count may be fitted to a model that provokes the deactivation of growing polymer chains. All of these properties need to use a specific kinetic mechanism that assumes a low activity of the developing polymer chains containing one E/VCH unit, the Zr–C$_2$H$_5$ group, in the E insertion process into the Zr–C bond. The copolymers obtained can be dissolved in conventional organic solvent and they have excellent thermal stability and crystalline temperature ($\Delta H_m$), their melting temperature (Tm) varies from 109 to 126 °C, and $\Delta H_m$ varies from 80 to 128 (J/g). The Mw of the E/VCH copolymers was lower at the beginning of the reaction but gradually rose with $t_p$. A narrow MWD which is nonetheless higher than two suggests numerous active [Zr]/[C*] sites in the catalytic system.

**Supplementary Materials:** The following supporting information can be downloaded at: https://www.mdpi.com/article/10.3390/polym14030459/s1, Figure S1: Change of molecular distribution of E/VCH copolymers with polymerization time; Figure S2: HNMR Spectra’s of the E/VCH copolymer; Figure S3: The plot of molVCH/molcat vs. time, and Differentiate; Figure S4: The plot of molE/molcat vs. time, and Differentiate; Table S1: Calculation of $R_p$VCH and $k_p$VCH in the ethylene-VNB copolymerization; Table S2. Calculation of $R_p$E and $k_p$E in the ethylene-VCH copolymerization.

**Author Contributions:** Conceptualization, A.A. and A.N.; methodology, A.A.; software, T.R. and T.A.; validation, A.A., M.I., Z.-K.Z. and M.W.U.; formal analysis, A.U.R. and A.A.K.; investigation, A.A.; resources, Z.F.; data curation, L.G.; writing—original draft preparation, A.A.; writing—review and editing, A.A., A.N., L.G. and Z.F.; visualization, A.A., A.A.K.; supervision, L.G.; Z.F.; project administration, L.G.; funding acquisition, L.G. All authors have read and agreed to the published version of the manuscript.

**Funding:** This work was supported by National Natural Science Foundation of China (51803081).

**Institutional Review Board Statement:** Not applicable.

**Informed Consent Statement:** Not applicable.

**Data Availability Statement:** Not applicable.

**Acknowledgments:** The authors are thankful to the National Natural Foundation of China (51803081) for their financial support.

**Conflicts of Interest:** The representative authors have no conflict of interest to disclose in any capacity, either competing or financial.

**References**

1. Cueny, E.S.; Sita, L.R.; Landis, C.R. Quantitative Validation of the Living Coordinative Chain-Transfer Polymerization of 1-Hexene Using Chromophore Quench Labeling. *Macromolecules* 2020, 53, 5816–5825. [CrossRef]
2. Naga, N.; Tsuchiya, G.; Toyota, A. Synthesis and properties of polyethylene and polypropylene containing hydroxylated cyclic units in the main chain. *Polymer* 2006, 47, 520–526. [CrossRef]
3. Coran, A.Y.; Patel, R. Rubber-thermoplastic compositions. Part I. EPDM-polypropylene thermoplastic vulcanizates. *Rubber Chem. Technol.* 1980, 53, 141–150. [CrossRef]
4. Awais, M.; Omar, M.M.; Munir, A.; Ajmal, M.; Hussain, S.; Ahmad, S.A.; Ali, A. Co-gasification of different biomass feedstock in a pilot-scale (24 kWe) downdraft gasifier: An experimental approach. *Energy* 2022, 238, 121821. [CrossRef]
5. Jamil, M.I.; Wang, Q.; Ali, A.; Hussain, M.; Aziz, T.; Zhan, X.; Zhang, Q. Slippery Photothermal Trap for Outstanding Deicing Surfaces. *J. Bionic Eng.* 2021, 18, 548–558. [CrossRef]
6. Kim, D.-G.; Bell, A.; Register, R.A. Living Vinyl Addition Polymerization of Substituted Norbornenes by at-Bu3P-Ligated Methylpalladium Complex. *ACS Macro Lett.* 2015, 4, 327–330. [CrossRef]
7. Ali, A.; Nadeem, M.; Lu, J.; Moradian, J.M.; Rasheed, T.; Aziz, T.; Maouche, C.; Guo, Y.; Awais, M.; Zhiqiang, F. Rapid kinetic evaluation of homogeneous single-site metallocone catalysts and cyclic diene: How do the catalytic activity, molecular weight, and diene incorporation rate of olefins affect each other? RSC Adv. 2021, 11, 31817–31826. [CrossRef]

8. Chen, E.Y.-X.; Marks, T.J. Cocrystallates for metal-catalyzed olefin polymerization: Activators, activation processes, and structure-activity relationships. Chem. Rev. 2000, 100, 1391–1434. [CrossRef]

9. McKnight, A.L.; Waymouth, R.M. Group 4 ansa-cyclopentadienyl-amido catalysts for olefin polymerization. Chem. Rev. 1998, 98, 2587–2598. [CrossRef]

10. Muhammad, N.; Zhang, Y.; Li, W.; Zhao, Y.G.; Ali, A.; Subhani, Q.; Mahmud, T.; Liu, J.; Cui, H.; Zhu, Y. Determination of nitenpyram and 6-chloronicotinic acid in environmental samples by ion chromatography coupled with online photochemically induced fluorescence detector. J. Sep. Sci. 2018, 41, 4096–4104. [CrossRef]

11. Aziz, T.; Zheng, J.; Jamil, M.I.; Fan, H.; Ullah, R.; Iqbal, M.; Ali, A.; Khan, F.U.; Ullah, A. Enhancement in Adhesive and Thermal Properties of Bio-based Epoxy Resin by Using Eugenol Grafted Cellulose Nanocrystals. J. Inorg. Organomet. Polym. Mater. 2021, 31, 3290–3300. [CrossRef]

12. Faingol’d, E.; Saratovskikh, S.; Panin, A.; Babkina, O.; Zharkov, I.; Garifullin, N.; Shilov, G.; Bravaya, N. Ethylene/propylene and ethylene/propylene/5-ethylidene-2-norbornene copolymerizations on metallocene/(2,6-tBu2PhO-)AlbBu2 catalyst systems. Polymer 2021, 220, 123559. [CrossRef]

13. Aziz, T.; Iqbal, M.; Ullah, R.; Jamil, M.I.; Raheel, M.; Ali, A.; Khan, F.U.; Ullah, A.; Wazir, N. Improving Adhesive Properties of Cellulose Nanocrystals Modifying By 3-Glycidoxypropyltrimethoxy Silane (KH-560) Coupling Agents. Biomed. J. Sci. Tech. Res. 2021, 34, 005492. [CrossRef]

14. Kaminsky, W.; Fernandes, M. Discovery and development of metallocone-based polyolefins with special properties. Polyolefins J. 2015, 2, 1–16.

15. Desert, X.; Carpentier, J.-F.; Kirillov, E. Quantification of active sites in single-site group 4 metal olefin polymerization catalysis. Coord. Chem. Rev. 2019, 386, 50–68. [CrossRef]

16. Pittman, C.U. The discovery of metallocone- and metallocone-like addition polymers. J. Inorg. Organomet. Polym. Mater. 2005, 15, 33–55. [CrossRef]

17. Naseer, M.A.; Tufail, M.K.; Ali, A.; Hussain, S.; Khan, U.; Jin, H.-B. Review on Computational-Assisted to Experimental Synthesis, Interfacial Perspectives of Garnet-Solid Electrolytes for All-Solid-State Lithium Batteries. J. Electrochem. Soc. 2021, 168, 060529. [CrossRef]

18. Rasool, G.; Shafiq, A.; Chu, Y.-M.; Bhutta, M.S.; Ali, A. Optimal Homotopic Exploration of features of Cattaneo-Christov model in Second Grade Nanofluid flow via Darcy-Forchheimer medium subject to Viscous Dissipation and Thermal Radiation. Comb. Chem. High Throughput Screen. 2021. [CrossRef]

19. Bochmann, M. Kinetic and mechanistic aspects of metallocone polymerisation catalysts. J. Organomet. Chem. 2004, 689, 3982–3998. [CrossRef]

20. Wondimagen, T.; Wang, D.; Razavi, A.; Ziegler, T. Computational design of C 2-symmetric metallocone-based catalysts for the synthesis of high molecular weight polymers from ethylene/propylene copolymerization. Organometallics 2008, 27, 6434–6439. [CrossRef]

21. Moscat, B.M.; Zhu, B.; Landis, C.R. Mechanistic investigations into the behavior of a labeled zirconocene polymerization catalyst. Organometallics 2012, 31, 2097–2107. [CrossRef]

22. Moradian, J.M.; Mi, J.-L.; Dai, X.; Sun, G.-F.; Du, J.; Ye, X.-M.; Yong, Y.-C. Yeast-induced formation of graphene hydrogels anode for efficient xylose-fueled microbial fuel cells. Chemosphere 2021, 291, 132963. [CrossRef] [PubMed]

23. Lin, S.; Tagge, C.D.; Waymouth, R.M.; Nele, M.; Collins, S.; Pinto, J. Kinetics of propylene polymerization using bis (2-phenylindenyl) zirconium dichloride/methylaluminoxane. J. Am. Chem. Soc. 2000, 122, 11275–11285. [CrossRef] [PubMed]

24. Ghiotto, F.; Pateraki, C.; Severn, J.R.; Friederichs, N.; Bochmann, M. Rapid evaluation of catalysts and MAO activators by kinetics: What controls polymer molecular weight and activity in metallocene/MAO catalysts? Dalton Trans. 2013, 42, 9040–9048. [CrossRef] [PubMed]

25. Moscat, B.M.; Zhu, B.; Landis, C.R. Mechanistic investigations into the behavior of a labeled zirconocene polymerization catalyst. Organometallics 2012, 31, 2097–2107. [CrossRef]

26. Moradian, J.M.; Mi, J.-L.; Dai, X.; Sun, G.-F.; Du, J.; Ye, X.-M.; Yong, Y.-C. Yeast-induced formation of graphene hydrogels anode for efficient xylose-fueled microbial fuel cells. Chemosphere 2021, 291, 132963. [CrossRef] [PubMed]

27. Lin, S.; Tagge, C.D.; Waymouth, R.M.; Nele, M.; Collins, S.; Pinto, J. Kinetics of propylene polymerization using bis (2-phenylindenyl) zirconium dichloride/methylaluminoxane. J. Am. Chem. Soc. 2000, 122, 11275–11285. [CrossRef] [PubMed]

28. Ghiotto, F.; Pateraki, C.; Severn, J.R.; Friederichs, N.; Bochmann, M. Rapid evaluation of catalysts and MAO activators by kinetics: What controls polymer molecular weight and activity in metallocene/MAO catalysts? Dalton Trans. 2013, 42, 9040–9048. [CrossRef] [PubMed]

29. Ali, A.; Jamil, M.I.; Uddin, A.; Hussain, M.; Aziz, T.; Tufail, M.K.; Guo, Y.; Jiang, B.; Fan, Z.; Guo, L. Kinetic and thermal study of ethylene-propylene copolymerization catalyzed byansa-zirconocene activated with Alkylaluminoxide/borate: Effects of linear and branched alkylaluminium compounds as cocatalyst. J. Polym. Res. 2021, 28, 186. [CrossRef]
30. Röll, W.; Brintzinger, H.H.; Rieger, B.; Zolk, R. Stereo- and Regioselectivity of Chiral, Alkyl-substituted ansa-Zirconocene Catalysts in Methylaluminoxane-activated Propene Polymerization. *Angew. Chem. Int. Ed. Engl.* **1990**, *29*, 279–280. [CrossRef]

31. Ali, A.; Akram, M.A.; Guo, Y.; Wu, H.; Liu, W.; Khan, A.; Liu, X.; Fu, Z.; Fan, Z. Ethylene–propylene copolymerization and their terpolymerization with dienes using ansa-Zirconocene catalysts activated by borate/aluminoxane. *J. Macromol. Sci. Part A* **2020**, *57*, 156–164. [CrossRef]

32. Jiang, B.; Zhang, B.; Guo, Y.; Ali, A.; Guo, W.; Fu, Z.; Fan, Z. Effects of titanium dispersion state on distribution and reactivity of active centers in propylene polymerization with MgCl2-supported Ziegler-Natta catalysts: A kinetic study based on active center counting. *ChemCatChem* **2020**, *12*, 5140–5148. [CrossRef]

33. Akram, M.A.; Liu, X.; Jiang, B.; Zhang, B.; Ali, A.; Fu, Z.; Fan, Z. Effect of alkylaluminum cocatalyst on ethylene/1-hexene copolymerization and active center distribution of MgCl2-supported Ziegler-Natta catalyst. *J. Macromol. Sci. Part A* **2021**, *58*, 539–549. [CrossRef]

34. Ali, A.; Tufail, M.K.; Jamil, M.I.; Yaseen, W.; Iqbal, N.; Hussain, M.; Ali, A.; Aziz, T.; Fan, Z.; Guo, L. Comparative Analysis of Ethylene/Diene Copolymerization and Ethylene/Propylene/Diene Terpolymerization Using Ansa-Zirconocene Catalyst with Alkylaluminum/Borate Activator: The Effect of Conjugated and Nonconjugated Dienes on Catalytic Behavior and Polymer Microstructure. *Molecules* **2021**, *26*, 2037.

35. Chowdhury, S.I.; Tanaka, R.; Nakayama, Y.; Shiono, T. Copolymerization of norbornene and conjugated dienes using anilinonaphthoquinone-ligated nickel complexes. *Polymer* **2020**, *187*, 122094. [CrossRef]

36. Choi, S.-S.; Kim, Y.-K. Analysis of 5-ethylidene-2-norbornene in ethylene-propylene-diene terpolymer using pyrolysis-GC/MS. *Eur. Polym. J.* **1995**, *30*, 867–875. [CrossRef]

37. Ahmadjo, S.; Arabi, H.; Nekoomanesh, M.; Zohuri, G.H.; Mortazavi, M.M.; Naderi, G. Terpolymerization of Ethylene, Propylene, and 5-Ethylidene-2-norbornene: Heterogeneous High-Ethylene EPDM Thermoplastic Elastomers. *J. Macromol. Sci. Part A* **1985**, *29*, 156–164. [CrossRef]

38. Kaminsky, W.; Miri, M. Ethylene propylene diene terpolymers produced with a homogeneous and highly active zirconium (IV) catalysts. *RSC Adv.* **2016**, *6*, 59590–59599. [CrossRef]

39. Kamaras, W.; Míguez Hernández, M.a.T.; Perez-Camacho, O. Activation of Cp2ZrX2 (X = Me, Cl) by methylaluminoxane as studied by electrospray ionization mass spectrometry: Relationship to polymerization catalysis. *Macromolecules* **2010**, *43*, 707–714. [CrossRef]

40. Collins, S.; Linnolahti, M.; Zamora, M.G.; Zijlstra, H.S.; Rodriguez Hernández, M.a.T.; Perez-Camacho, O. Activation of Cp2ZrX2 (X = Me, Cl) by methylaluminoxane as studied by electrospray ionization mass spectrometry: Relationship to polymerization catalysis. *Macromolecules* **2010**, *43*, 707–714. [CrossRef]

41. Marques, M.; Yu, Z.; Rausch, M.D.; Chien, J.C. Olefin terpolymerizations. II. 4-vinylcyclohexene and cyclooctadiene. *J. Polym. Sci.* **1995**, *33*, 2587–2593. [CrossRef]

42. Ali, A.; Uddin, A.; Jamil, M.I.; Shen, X.; Abbas, M.; Aziz, T.; Hussain, M.; Hussain, S.; Fang, R.; Fan, Z. Kinetics and mechanistic investigations of ethylene-propylene copolymerizations catalyzed with symmetrical metallocones and activated by TIBA/borate. *J. Organomet. Chem.* **2021**, *949*, 121929. [CrossRef]

43. Marathe, S.; Sivaram, S. Regioselective copolymerization of 5-vinyl-2-norbornene with ethylene using zincocenocenemethylaluminoxane catalysts: A facile route to functional polyolefins. *Macromolecules* **1994**, *27*, 1083–1086. [CrossRef]

44. Lasarov, H.; Paskenen, T.T. Ethylene-Norbornene Terpolymerization with 5-Vinyl-2-norbornene Using Single-Site Catalysts. *Macromol. Rapid Commun.* **2001**, *22*, 434–438. [CrossRef]

45. Leone, G.; Zanchin, G.; De Stefano, D.; Lorber, C.; Bertini, F. Semibatch Terpolymerization of Ethylene, Propylene, and 5-Ethylidene-2-norbornene: Heterogeneous High-Ethylene EPDM Thermoplastic Elastomers. *J. Polym. Sci. Part A Polym. Chem.* **2016**, *54*, 5881–5894. [CrossRef]

46. Ali, A.; Uddin, A.; Jamil, M.I.; Shen, X.; Abbas, M.; Aziz, T.; Hussain, M.; Hussain, S.; Fang, R.; Fan, Z. Kinetics and mechanism of metalloene-catalyzed olefin polymerization: Comparison of ethylene, propylene homopolymers and their copolymerization. *J. Polym. Sci. Part A* **2017**, *55*, 867–875. [CrossRef]