Stellar Mass—Halo Mass Relation and Star Formation Efficiency in High-Mass Halos*

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Abstract—We study relation between stellar mass and halo mass for high-mass halos using a sample of galaxy clusters with accurate measurements of stellar masses from optical and infrared data and total masses from X-ray observations. We find that stellar mass of the brightest cluster galaxies (BCGs) scales as $M_{\ast,BCG} \propto M_{500}^{0.500}$ with the best fit slope of $\alpha_{BCG} \approx 0.4 \pm 0.1$. We measure scatter of $M_{\ast,BCG}$ at a fixed $M_{500}$ of $\approx 0.2$ dex. We show that stellar mass-halo mass relations from abundance matching or halo modelling reported in recent studies underestimate masses of BCGs by a factor of $\sim 2-4$. We argue that this is because these studies used stellar mass functions (SMF) based on photometry that severely underestimates the outer surface brightness profiles of massive galaxies. We show that $M_{\ast} - M$ relation derived using abundance matching with the recent SMF calibration by Bernardi et al. (2013) based on improved photometry is in a much better agreement with the relation we derive via direct calibration for observed clusters. The total stellar mass of galaxies correlates with total mass $M_{500}$ with the slope of $\approx 0.6 \pm 0.1$ and scatter of $0.1$ dex. This indicates that efficiency with which baryons are converted into stars decreases with increasing cluster mass. The low scatter is due to large contribution of satellite galaxies: the stellar mass in satellite galaxies correlates with $M_{500}$ with scatter of $\approx 0.1$ dex and best fit slope of $\alpha_{\text{sat}} \approx 0.8 \pm 0.1$. We show that for a fixed choice of the initial mass function (IMF) total stellar fraction in clusters is only a factor of $3-5$ lower than the peak stellar fraction reached in $M \approx 10^{12} M_{\odot}$ halos. The difference is only a factor of $\sim 1.5-3$ if the IMF becomes progressively more bottom heavy with increasing mass in early type galaxies, as indicated by recent observational analyses. This means that the overall efficiency of star formation in massive halos is only moderately suppressed compared to $L_*$ galaxies and is considerably less suppressed than previously thought. The larger normalization and slope of the $M_{\ast} - M$ relation derived in this study shows that feedback and associated suppression of star formation in massive halos should be weaker than assumed in most of the current semi-analytic models and simulations.

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INTRODUCTION

In hierarchical Cold Dark Matter (CDM) models of structure formation, galaxies are thought to form via dissipative processes within potential wells of dark matter-dominated halos (White and Rees 1978; Fall and Efstathiou 1980; Blumenthal et al. 1982, 1984). Cooling leads to condensation of baryons towards the center of their parent halo (e.g., Rees and Ostriker 1977) where they reach conditions suitable for star formation. Understanding efficiency with which halos convert their baryons into stars is one of the central problems in modelling galaxy formation. Results of abundance matching of halo mass function to the stellar mass function of galaxies showed that this efficiency peaks at halo masses of $M \approx 10^{12} M_{\odot}$ but is quickly decreasing at both smaller and larger masses (e.g., Conroy and Wechsler 2009; Guo et al. 2010). Remarkably, this peak mass is almost independent of redshift (Yang et al. 2012; Behroozi et al. 2013a). Even at the peak of efficiency, observed masses of

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cold gas and stars in galaxies corresponds to only \(\approx 20–30\%\) of the mass of baryons which should have been potentially available in \(M \approx 10^{12} \, M_\odot\) halos. The implied low star formation efficiencies are widely believed to be due to strong feedback processes, which suppress star formation and blow out a large fraction of gas out of host halos.

In particular, it is commonly acknowledged that the AGN feedback plays a key role in shaping properties of baryons in massive halos and in setting their star formation efficiency (see, e.g., Silk and Rees (1998) and McNamara and Nulsen (2007) for a recent review). Semi-analytical models showed that without AGN feedback one cannot reproduce the high mass end of stellar mass function (e.g., Benson et al. 2003; Croton et al. 2006). Simulations carried out over 15–15 years clearly showed that without strong AGN feedback stellar fractions in groups and clusters are overestimated by a factor of \(\sim 2–3\) compared to observations (see Kravtsov and Borgani (2012) for a recent review). Inclusion of strong AGN feedback in simulations using phenomenological recipes indeed lowers stellar fractions by a significant factor (e.g., McCarthy et al. 2010, 2011; Planelles et al. 2013; Martizzi et al. 2012, 2013; Ragone-Figueroa et al. 2013).

Although these results are encouraging, they are not yet conclusive. Details of how AGN feedback affects evolution of massive galaxies and properties of their gaseous halos are not yet fully understood. Implementations of AGN feedback in semi-analytic models and cosmological simulations are thus associated with significant systematic uncertainties, which means that results of model calculations need to be thoroughly tested against observations. Group and cluster scale halos provide a unique way of testing models because stellar masses of galaxies, halo gas content, and halo mass all can be estimated from observations fairly reliably.

In this paper, we use a sample of nine clusters with carefully measured stellar masses and total masses to calibrate efficiency of star formation and stellar mass—halo mass relation in massive halos. We combine this sample with 12 clusters with similar data from a recent study of Gonzalez et al. (2013) to improve the statistics in calibrations of trends. Although stellar content of clusters was investigated in a number of recent studies (Gonzalez et al. 2007, 2013; Laganá et al. 2013; Bydzynski et al. 2014), most of these works focused on the total stellar and hot gas content only to estimate total baryon budget of clusters, rather than on stellar mass—halo mass relation of galaxies specifically. In this study we consider both the total stellar mass within halos and masses of the BCG and satellite galaxies separately, because transition from galaxy-sized halos to groups and clusters is accompanied by increasing fraction of stellar mass in satellite galaxies.

In addition, the fraction of stellar mass in the outer regions around central galaxies also increases with increasing halo mass. In galaxy clusters the outer regions of the brightest cluster galaxy are often called the intra-cluster light (ICL) and are estimated to contain a significant fraction of the BCG mass and up to \(\sim 20–40\%\) of the total stellar mass within the virial radius (Zibetti et al. 2003; Gonzalez et al. 2007; Skibba et al. 2007; Gonzalez et al. 2013; McGee and Balogh 2010). Thus, the outer profiles of BCGs need to be properly accounted for when considering stellar content of clusters. Profiles at large radii can, however, be easily missed or under-estimated in observations due to their low surface brightness and challenges in estimating background around large massive galaxies in crowded environments.

In this study we use stellar masses measured in re-analysis of the SDSS data with a careful treatment of background, which allows us to recover the low surface brightness outer profiles of galaxies out to \(\approx 100–300\) kpc. We use these measurements along with X-ray estimates of total cluster mass to calibrate stellar mass—halo mass relation and stellar fractions of high mass halos.

The paper is organized as follows. We present our stellar surface density and mass measurements in Section 2. We show that stellar masses of BCGs in nearby clusters based on the standard SDSS photometry are underestimated by a factor of \(\sim 2–4\). At the same time, our measurements are in good agreement with luminosities derived by Bernardi et al. (2013) using re-analysis of the SDSS data with improved estimate of background. We show that stellar mass of BCGs continues to increase at the outermost measured radii in most clusters.

We present calibrations of stellar mass—halo mass relation for a combined sample of 21 clusters in Section 3. We compare our observational calibrations with expectations from the halo abundance ansatz and show that they are in reasonable agreement if the recent calibration of the SMF by Bernardi et al. (2013) is used in the latter. In Section 3.2 we show that BCG size correlates with cluster halo virial radius and extends the corresponding correlation of smaller mass galaxies.

We discuss interpretation of our stellar mass—halo mass relation in terms of efficiency of star formation in halos of different mass in Section 4. We show that inclusion of the outer regions of BCGs in stellar mass measurement considerably increases the stellar mass and star formation efficiency estimates. We also point out that if the initial mass function of stars becomes substantially more bottom-heavy in massive early type galaxies, as indicated by a number of recent
observational analyses, the star formation efficiency in cluster halos is only a factor of \(\sim 2-3\) lower than the efficiency of \(M \approx 10^{12} M_\odot\) halos. We discuss our results in Section 5, comparing them with results of previous studies of stellar fraction as a function of mass in Section 5.1. We discuss implications of our results for the strength of feedback in semi-analytic models and cosmological simulations in Section 5.2. We summarize our results and conclusions in Section 6.

Unless otherwise noted, throughout this paper we assume a flat \(\Lambda\)CDM model with parameters \(\Omega_m = 1 - \Omega_\Lambda = 0.27, \Omega_b = 0.0469, h = H_0/(100 \text{ km s}^{-1} \times \text{Mpc}^{-1}) = 0.7, \sigma_8 = 0.82, \) and \(n_s = 0.95\) compatible with combined constraints from WMAP, BAO, SNe, and cluster abundance (Vikhlinin et al. 2009b; Komatsu et al. 2011; Hinshaw et al. 2013). Total masses are defined within radius enclosing a particular overdensity (500 or 200) with respect to the critical density at redshift of observation, which is indicated by a corresponding subscript (\(M_{500}\) or \(M_{200}\)). Throughout the paper we assume the Chabrier (2003) IMF in the calculation of stellar masses, except in Section 4.1 where we explore sensitivity of stellar fractions to IMF variation.

**STELLAR MASSES OF GROUP AND CLUSTER GALAXIES**

To calibrate the stellar mass—halo mass relation on the high mass end, we use two sets of measurements for a combined sample of 21 clusters with \(z \lesssim 0.1\) spanning the total mass range of \(M_{500} \approx (0.5-15) \times 10^{14} M_\odot\). The clusters in the sample have individual measurements of stellar masses, which include measurements of low surface brightness outer regions of massive galaxies, and high-quality X-ray data, which are used to get accurate estimates of the total masses of individual clusters.

The first set is taken from a recent study by Gonzalez et al. (2013), hereafter G13, who used re-analysis of the \(I\) band photometry for a subset of 12 clusters from Gonzalez et al. (2007) complemented with the XMM-Newton X-ray data. The total mass, \(M_{500}\), for these clusters is estimated using X-ray temperature obtained by the spectral fit within the radial range \((0.15-0.5) R_{500}\) via an iterative procedure and a fitting formula of Vikhlinin et al. (2009a). The total masses derived by G13 are in good agreement with the masses derived by Vikhlinin et al. (2006) for the same clusters, but are slightly lower by an average of \(\approx 8\%\). This offset is independent of mass and reflects a small systematic difference between *Chandra* and XMM-Newton cluster temperature measurements (Vikhlinin et al. 2005). Its magnitude is too low to affect our results and conclusions. The total \(I\)-band luminosities of galaxies were derived from drift-scan observations at the Las Campanas 1 m Swope telescope by carefully modelling profiles of galaxies to large radii and low surface brightness, as detailed in Gonzalez et al. (2005).

The second set of measurements is new and was derived using the SDSS data for nine nearby \((z < 0.1)\) clusters, all of which fall within the SDSS footprint and have high-quality Chandra X-ray data. The sample was chosen to span a wide range of total masses (see Table 1) and to avoid highly disturbed systems in which we cannot assume spherical symmetry. The total masses, \(M_{500}\), were derived using robust, low-scatter mass proxy \(Y_X\) (Kravtsov et al. 2006) derived from the Chandra observations, as described in Vikhlinin et al. (2009a), except for Abell 1991, MKW 4, RXJ 1159+5531. For the latter three clusters the gas and total masses were estimated from *Chandra* X-ray data using the identical analysis. We describe the procedure used to derive the stellar masses next.

**Stellar Mass Measurements for Nine Clusters Using the SDSS Data**

The stellar masses were measured using raw images and corresponding calibration data from the Sloan Digital Sky Survey Release 8 in \(g, r, \) and \(i\) bands \(^1\) in the \(38.6' \times 42.2'\) aligned mosaic fields centered on the brightest galaxy in each cluster. The mosaic images in each band were constructed by combining together four fields of the same SDSS drift scan (run) that contain cluster BCG into \(2048 \times 6933\) pixel strips and then gluing together three neighboring strips. These three strips came from different runs and thus have patterns of background non-uniformities. The strongest background non-uniformities in the SDSS images are in the scan direction (\(y\)). Fortunately, the individual SDSS scans overlap, and therefore the difference in the background patterns in the scan direction can be eliminated. We achieved this by fitting a low-order polynomial to the difference in the 1D profiles in the overlapping region of the neighboring strips, and subtracted that fit from the strips adjacent to that containing the brightest cluster galaxy. After the strips were joined, we subtracted the global background profile from the whole mosaic image. The global background was estimated in a region of width equal to \(300-500\) pixels and length equal to the entire mosaic in the \(y\)-direction, chosen in

\(^1\)http://www.sdss.org/dr8/

\(^2\)Corresponding to physical areas of \(\approx 2 \times 2 R_{500}\) for most clusters, and \(\approx 1.6 \times 1.6 R_{500}\) for MKW4, \(\approx 3.4 \times 3.8 R_{500}\) for Abell 1991, \(\approx 6.0 \times 6.8 R_{500}\) RXJ 1159.
Table 1. Nine galaxy clusters with the SDSS stellar mass measurements

| Cluster name | $z$     | $R_{500}$ | $M_{500}$ | $R_{out}$ | $M_{*,BCG}(<R_{out})$ | $M_{*,BCG}$ | $M_{*,non-BCG}$ | $r_{1/2}$ | $r_{1/2}(<R_{out})$ |
|--------------|---------|-----------|-----------|-----------|----------------------|-------------|-----------------|-----------|-------------------|
| A2142        | 1539    | 11.96 ± 0.200 | 15.60     | 220       | 1.95 ± 0.17$^a$      | 3.12 ± 0.36 | 12.22 ± 1.58    | 179 ± 41  | 52 ± 9            |
| A2029        | 1387    | 8.64 ± 0.140 | 10.30     | 271       | 3.42 ± 0.20          | 4.14 ± 0.30 | 8.21 ± 1.05     | 84 ± 7    | 44 ± 6            |
| A85          | 1235    | 5.98 ± 0.070 | 7.00      | 308       | 2.49 ± 0.21          | 3.06 ± 0.30 | 5.28 ± 0.74     | 174 ± 24  | 69 ± 19           |
| A1795        | 1196    | 5.46 ± 0.060 | 5.34      | 210       | 1.22 ± 0.09          | 1.47 ± 0.13 | 4.01 ± 0.75     | 99 ± 10   | 47 ± 9            |
| MKW3s        | 873     | 2.09 ± 0.030 | 2.35      | 116       | 0.73 ± 0.03$^b$      | 0.79 ± 0.05 | 1.89 ± 0.49     | 34 ± 4    | 22 ± 3            |
| A2052        | 840     | 1.84 ± 0.030 | 1.86      | 186       | 1.08 ± 0.07          | 1.26 ± 0.11 | 2.22 ± 0.47     | 53 ± 3    | 31 ± 4            |
| A1991        | 748     | 1.33 ± 0.037 | 1.34      | 117       | 1.05 ± 0.05          | 1.09 ± 0.06 | 1.77 ± 0.41     | 37 ± 2    | 25 ± 2            |
| MKW4         | 568     | 0.56 ± 0.013 | 0.46      | 133       | 0.87 ± 0.04          | 0.91 ± 0.05 | 0.97 ± 0.29     | 29 ± 2    | 20 ± 2            |
| RXJ1159      | 568     | 0.59 ± 0.028 | 0.47      | 142       | 1.10 ± 0.05          | 1.38 ± 0.14 | 0.47 ± 0.18     | 31 ± 5    | 15 ± 2            |

$^a$ The stellar masses of the second brightest galaxy in A2142 are: $M_*(<R_{out}) = 7.8 ± 0.43 \times 10^{11} M_\odot$, where $R_{out} = 101$ kpc, and total mass extrapolated to infinity $M_{*,tot} = 8.50 ± 0.63 \times 10^{11} M_\odot$.

$^b$ The stellar masses of the second brightest galaxy in MKW3s are: $M_*(<R_{out}) = 3.6 ± 0.16 \times 10^{11} M_\odot$, where $R_{out} = 68$ kpc, and total mass extrapolated to infinity $M_{*,tot} = 3.78 ± 0.39 \times 10^{11} M_\odot$.

The images were de-blended from nearby stars and galaxies and appropriate mask regions were created in order to subtract contribution from remaining foreground/background objects (stars, galaxies and artefacts). Radial surface brightness in different bands and $(g-r)$ color profiles of the BCGs were then extracted from the de-blended and masked mosaic images.

In order to take into account possible additional residual variations of the background across the field, we fitted the quadratic model for residual background, $f(R) = C_0 + C_2 R^2$, where $R$ is the radial distance from the BCG center, during the profile extraction. Note that all linear and bilinear background components are averaged out in the azimuthal profile, and therefore thus defined $f(R)$ represents the lowest-order non-constant local background adjustment to the galaxy light profile. The $C_0$ and $C_2$ coefficients are determined by fitting the data in the at $R \gtrsim 600$–1400 pixels ($\gtrsim 4''$–$9''$), where the contribution of the BCG light is negligible. The best-fit $f(R)$ model is then interpolated to smaller radii, where the BCG profile measurements are typically done, $\lesssim 3.5''$. We evaluated the residual background uncertainties as a function of radius by applying this procedure to the SDSS mosaic images of the same size centered on random regions in the SDSS data that do not contain known nearby clusters. This test shows that the residual $r$-band background uncertainties in our BCG profiles are 28.4 mag arcsec$^{-2}$ at $R = 2'$, and 28.8 mag arcsec$^{-2}$ at $4'$. The image mosaic and background estimation procedure described above was done for each BCG galaxy of the nine clusters in our sample and for second brightest galaxy in Abell 2142 and MKW 3s. For satellite galaxies galaxy surface brightness profile plus a constant background, with corresponding masks and de-blending when needed, was measured within fields of 400 pix size centered on each galaxy. In a few difficult cases (out of several thousand total galaxies measured) the profiles were measured using extended regions of $\approx 600$–1000 pixels.

After subtracting the best-fit local background model, the BCG brightness profiles in $g$, $r$, and $i$ bands were obtained for all BCGs in our cluster sample. Conversion from counts on the SDSS images to apparent AB magnitudes was done following the standard procedure. The apparent magnitudes were then converted to the absolute magnitudes using $m - M_A + K(z) + EC(z) + DM(z, M, L, h)$, where $A$, $K(z)$, $EC(z)$, $DM$ are the Galactic absorption correction from the Schlegel et al. (1998) dust map individual for each cluster, $K$-correction, evolutionary correction and distance modulus. For galaxies

\[3\text{See http://www.sdss.org/dr7/algorithms/fluxcal.html}\]
The total magnitude of galaxy is estimated by extrapolating the model profile to infinity.

In Abell 2142 a special care needs to be taken in deriving the mass of the BCG, because the cluster contains a second bright galaxy of somewhat smaller luminosity near the BCG. We have de-blended the second bright galaxy by first deriving the profile of the BCG with the second brightest galaxy masked with a circular aperture of radius $53'' \approx 87$ kpc. The resulting surface brightness profile was fit with the triple Sérsic profile. This profile was then was subtracted from the image and the circular region of radius $75'' \approx 123$ kpc around the center of the BCG was masked out. The profile of the second brightest galaxy was then derived from the resulting image. In this procedure, any stellar envelope of the second brightest galaxy at large radii will be assigned to the BCG. To test for potential effect of such contribution, we have also recalculated BCG mass decreasing the stellar mass at $r > 170$ kpc by a factor of two. We have checked that all of the scaling relations measured below do not change if such reduced BCG mass is used for Abell 2142. MKW3s cluster has also a bright galaxy close to the BCG. In this case, the BCG mass was computed in a similar way to that of Abell 2142, but with preliminary profile of the second galaxy measured at small radii subtracted before measurement of the BCG profile. The BCG profile was then measured with a circle of radius $58'' \approx 50$ kpc masked around the second brightest galaxy. In this case, the second brightest galaxy has significantly lower luminosity than BCG and such procedure is more appropriate. The measured BCG profile was then subtracted from the image and profiles of other galaxies were measured with circle of radius $190'' = 164$ kpc around BCG masked out.

The results are reported in Table 1, while Fig. 1 shows the surface density profiles of $r$-band luminosity for BCGs in nine clusters along with the three Sérsic component best fit. The figure shows that luminosity increases at the outermost measured radius, $R_{\text{out}}$, in all BCGs and shows how much of the total luminosity is contributed by extrapolation of the fit beyond $R_{\text{out}}$. In the following analysis, we will be using stellar masses measured by extrapolation of the triple-Sérsic fit to their profiles within $R_{\text{out}}$ to infinity. Such extrapolation is a standard practice in measurements of galaxy luminosity, but is of course somewhat uncertain as the actual profile at large radii may deviate from the extrapolated one. As a conservative estimate for how much the stellar mass could be underestimated, we have also computed total BCG stellar masses by extrapolating their profiles at $R > R_{\text{out}}$ as $\Sigma(R) = \Sigma(R_{\text{out}})/(R/R_{\text{out}})^{-2}$, i.e., profile approximately describing $\Sigma(R)$ of most galaxies at $R \approx R_{\text{out}}$ out to $R_{500}$. Such masses are on average $\approx 30\%$ larger than the $M_{*,\text{BCG}}$ masses in Table 1. We have checked that using such masses simply increases normalization of the best fit $M_{*,\text{BCG}} - M_{500}$ relation presented in Section 3.1 (Table 2 and Fig. 4) by $\approx 30\%$ ($\approx 1.5\sigma$) but does not change slope and

Fig. 1. (Color online) Profiles of $r$-band luminosity surface density of BCGs in nine clusters analyzed in this study, as indicated in the legend. Luminosities are multiplied by $R^2$ and profiles are displaced by a dex with respect to each other for clarity (the third from the top profile of BCG in Abell 85 is not shifted). The thick lines are the actual measured profiles shown out to the radius $R_{\text{out}}$ (see Table 1) where background errors reach 33%, while the long dashed thin lines show the best three Sérsic component fit.
Comparison with Other Luminosity Measurements

Figure 2 compares luminosities derived in our analysis described above with the luminosities calculated from the cmodel magnitudes from the SDSS DR7 pipeline, and with the re-analyses of the photometry by Simard et al. (2011) and Bernardi et al. (2013). The luminosities for the latter two studies were calculated from the Sérsic fits to the r-band data. The SDSS cmodel luminosities were computed using deV and exp magnitudes for the same galaxies from the SDSS DR7 database using Eq. (1) in Bernardi et al. (2010) and applying sky-subtraction correction given by Eq. (4) in the same paper.

Figure 2 shows that luminosities derived in our analysis are in reasonable agreement with luminosities of Bernardi et al. (2013), although the scatter between the two measurements is substantial. Luminosities from the cmodel magnitudes are biased low by a factor of ~2–4 and there is an indication that the bias increases with increasing luminosity. Luminosities derived from the absolute magnitudes reported by Simard et al. (2011) for five of our galaxies that can be found in their catalog are also biased low, although the magnitude of the bias is somewhat smaller than for the cmodel luminosities. This indicates that the bias is not due to a particular choice of the functional form used to fit surface brightness profiles. Note that similar biases were reported by Bernardi et al. (2013), who show that the cmodel and Simard et al. (2011) absolute magnitudes are biased high by ~0.7 and ~0.5 magnitudes, respectively, at the absolute magnitudes characteristic of the cluster BCGs ($M_r \sim -24$ to $-26$). These differences correspond to factors of $\approx 1.6$ and $\approx 1.9$ in luminosity difference and are comparable to the results shown in Fig. 2 for lower luminosity BCGs. Our results indicate that bias for the most luminous BCGs is even larger and reaches factors of $\approx 3–4$.

The origin of the bias is clear from the comparison of the surface brightness profiles shown in Fig. 3. In this figure we show the r-band luminosity surface density profiles for five galaxies for which there is corresponding photometry in the SDSS DR7 catalog along with the results of the Sérsic fits using the PyMorph method by Bernardi et al. (2013), and 2D Sérsic fits from the catalog of Simard et al. (2011). In the latter photometric redshifts of the galaxies were used to compute luminosities and radii for some of the galaxies. We have rescaled these to the proper spectroscopic redshifts used to derive luminosities in our study. Note that BCG of Abell 85 is absent from the Simard et al. (2011) catalog.

Figure 3 shows that standard SDSS photometry underestimates the luminosity density somewhat at small radii for all galaxies and severely underestimates the luminosity density at large radii for all galaxies. The best fit profiles of Simard et al. (2011) are not biased at small radii, but have equally large error at large radii. As shown by Lauer et al. (2007) and Bernardi et al. (2007), the main source of the bias is over-subtraction of background (see also He et al. 2013) that is estimated at radii that are too small for such luminous, extended galaxies in general, and BCGs in particular. Recently, Bernardi et al. (2013) and He et al. (2013) showed that this bias increases with increasing galaxy luminosity and significantly affects galaxies on the exponential part of the luminosity function ($L > L_*$). Bernardi et al. (2013) correct for this problem in their analysis and their best fit Sérsic profiles are in a much better agreement with the profiles derived in this study at large radii. The only exception is BCG in Abell 85, which has a very shallow outer profile that single Sérsic component does not fit well.
Overall our results confirm the bias underestimating luminosities by the SDSS photometric pipeline and the fact that bias increases with increasing galaxy luminosity. Comparisons indicate that luminosities derived using the single Sérsic fits with proper handling of sky background subtraction by Bernardi et al. (2013) are not significantly biased with respect to our photometric analysis.

**Measuring Luminosities of Satellite Galaxies**

In addition to the light of the BCG, we measure luminosities associated with other cluster galaxies as follows. We first construct a complete list of galaxies up to a cluster-centric radius of \(\approx 2^\circ - 4^\circ\) \((\approx 10 - 20 R_{500})\) from the SDSS photometric catalog using only objects detected with \(\geq 5\sigma\) significance in \(g\), \(r\), and \(i\) bands and which are classified as GALAXY in at least two of the three photometric bands. We have rejected all objects with saturated pixels and which are flagged as BRIGHT.

We use the selection criteria of Yasuda et al. (2001) to select only objects flagged in the SDSS catalog as PRIMARY, which avoids multiple detections in the overlap between adjacent scan lines in two strips and between adjacent frames. Furthermore, we use only isolated objects, child objects and NODEBLEND flagged objects in constructing the galaxy sample.

The object list is cleaned to remove background and foreground galaxies using tiling data from the SDSS spectroscopic catalog, which allows us to substantially reduce the statistical background for galaxies brighter than \(r = 17.5\) mag. We use the USNO B1 catalog to identify very bright stars in the field and mask out regions in which light from star affects photometry of galaxies.

In addition, regions containing visible prominent density peaks in galaxy distribution in the neighborhood of each cluster were masked. Furthermore, we use images from the ROSAT All Sky Survey to identify nearby clusters and mask out regions of diffuse X-ray sources from our analysis. This avoids any effect projecting substructure may have on the radial distribution of cluster galaxies.

As we discussed above, for bright galaxies the luminosity may be significantly underestimated if background is overestimated. Although the problem is most severe for the brightest galaxies, it can also affect luminosities of lower mass systems. We have compared total luminosities and colors obtained from the magnitudes in the SDSS catalog with values from our own re-analysis of photometry using profile fitting procedure similar to that described above for the BCG galaxies, except for lower luminosity galaxies we fitted two Sérsic components rather than three. The total galaxy luminosities in our re-analysis were obtained by extrapolating the best fit two-Sérsic profiles to infinity. We performed such re-analysis for all galaxies within \(6R_{500}\) of the cluster center and with \(L_r \geq (1.5 - 10) \times 10^9 L_\odot\) (the limit varied from cluster to cluster). The luminosities derived in this way are generally higher than luminosities from the SDSS photometry for galaxies with with absolute magnitudes of \(M_r \geq -21\) with difference increasing with increasing luminosity, consistent with results of Bernardi et al. (2013). We have fit a low-order polynomial for the luminosity dependence of the difference in magnitudes and applied this correction for low-luminosity galaxies below the threshold for our photometric re-analysis.

To estimate galaxy colors we integrated best fit surface brightness profiles models within aperture \(R_{col} = \max(R_{eff}, 5\, kpc)\), where \(R_{eff}\) was calculated from the \(R_{eff} - L_r\) relation of elliptical galaxies (e.g., Desroches et al. 2007). We find colors that are consistent with colors from the SDSS catalog. Given luminosities and colors, stellar masses are estimated using relation between \(M_*/L\) and color, as described in the next section.

Using the measured stellar masses we construct stellar mass function (SMF) of cluster galaxies. For each cluster, we estimate the number of galaxies in a given luminosity bin \(j\) as \(N_j = N_{a,j} - N_{b,j}S_a/S_b\), where \(N_{a,j}\) is the number of galaxies (cluster + field) within the cluster region, \(N_{b,j}\) is the number of galaxies in the background region, and \(S_a\) and \(S_b\) are the areas of cluster and field region, respectively. We choose the field region to estimate the background at \(R \approx 5 - 6 R_{500}\) from the cluster X-ray peak with area such that \(S_a/S_b \ll 1\), while cluster aperture is chosen to be a circle of radius \(0.7 R_{500}\) centered on the X-ray peak.

The SMF of cluster galaxies shows a prominent break and starts to decrease at stellar mass \(M_* \lesssim 1 - 5 \times 10^9 M_\odot\), which corresponds to apparent magnitude of \(m_r \approx 20.5\) (this break varies within this range from cluster to cluster in terms of stellar mass). We thus adopt completeness limit, \(M_{lim}\), for the stellar mass equal to twice the value of the break estimated for each cluster and fit Schechter form to the SMF for galaxies with \(M_* > M_{lim}\), excluding the BCG. The SMF normalized by total mass, \(d(N/M_{500})/dM_*\), of eight clusters, except MKW 4, can be described by the same Schechter function, \(d(N/M_{500})/dM_* \propto (M_*/M_{*,ch})^{\alpha} \exp(-[M_{*,ch}])\) \((x < 2.7)\) with normalization of \(6.15 \times 10^{-25}\), \(\alpha = -1.09\) and \(M_{sb} = 1.23 \times 10^{11} M_\odot\). Extrapolating the best fit functional fit to SMF below \(M_{lim}\), we estimate contribution of galaxies with \(M_* < M_{*,lim}\) to be \(\approx 10 - 20\%\) for eight of the clusters in our sample. MKW 4 is the nearest cluster in our sample and has the absolute magnitude
Table 2. Best fit parameters for power law fits

| Relation         | Slope     | Normalization | Scatter |
|------------------|-----------|---------------|---------|
| $M_{*,\text{BCG}} - M_{500}$ | 0.39 ± 0.17 | 12.15 ± 0.08 | 0.21 ± 0.09 |
| $M_{*,\text{sat}} - M_{500}$ | 0.87 ± 0.15 | 12.42 ± 0.07 | 0.10 ± 0.12 |
| $M_{*,\text{tot}} - M_{500}$ | 0.69 ± 0.09 | 12.63 ± 0.04 | 0.09 ± 0.05 |
| $M_{*,\text{BCG}} - M_{500}$ | 0.33 ± 0.11 | 12.24 ± 0.04 | 0.17 ± 0.03 |
| $M_{*,\text{sat}} - M_{500}$ | 0.75 ± 0.085 | 12.52 ± 0.03 | 0.10 ± 0.03 |
| $M_{*,\text{tot}} - M_{500}$ | 0.59 ± 0.08 | 12.71 ± 0.03 | 0.11 ± 0.03 |

The relations are fit by the power law $y = mx + c$, where $x = \log_{10} M_{500} - 14.5$ and $y = \log_{10} M_*$. We have derived these parameters by using likelihood maximization power law fit simultaneously for the slope, normalization, and scatter of the relation taking into account both errors in $M_{500}$ and $M_*$ (Hogg et al. 2010). All errors correspond to one standard deviation. The quoted scatter is in $y$ direction in dex. All masses are in $M_{\odot}$ and assume Chabrier IMF.

limit two magnitudes fainter than for other clusters. For this cluster we fit SMF of cluster galaxies with a double Schechter fit fixing the characteristic mass of bright galaxies to the above value for the rest of the clusters, but varying all other parameters. We derive best fit slope of the bright-end Schechter function of $\alpha_b = -0.66$; at the faint end the best fit slope and characteristic mass are $\alpha_i = -1.82$ and $M_{i,\text{lim}} = 9.05 \times 10^8 M_\odot$. Based on this fit, contribution of galaxies with $M_r < M_{r,\text{lim}}$ for MKW 4 is to be $\approx 26\%$ for the nine clusters in our sample. If SMFs in the other eight clusters have a similar upturn at small masses, we may be missing up to $\approx 25\%$ of stellar light in the estimate of the total stellar mass in satellite galaxies.

To measure projected (2D) radial distribution of galaxies we use only the galaxies with $M_r > M_{r,\text{lim}}$. We de-project the 2D profile by forward fitting a 3D $(\alpha, \beta, \gamma)$ profile model, $\rho(r) = A(r/R_s)^{-\alpha}(1 + [r/R_s]^\beta)^{-(\gamma - \alpha)/\beta}$ (Lauer et al. 1995; Zhao 1996) plus constant background, $B$, to the projected profile, where $\alpha$ controls the inner slope, $\beta$ controls the outer slope, and $\beta$ controls how fast the slope changes around $R = R_s$. We fix $\alpha = 0, \beta = 3$ in out fits and fit for normalization $A$, $R_s$, $\gamma$, and $B$. The best fit profiles are used to estimate stellar mass of non-BCG galaxies within a given 3D aperture (we use primarily $R_{500}$ in this study). The uncertainties in the model parameters ($A$, $R_s$, $\gamma$, and $B$) are fully propagated into the uncertainties in the 3D stellar mass contained in the stellar masses of non-central satellite galaxies.

From Luminosities to Stellar Mass

Converting luminosity to stellar mass requires assumptions about stellar mass-to-light ratio based either on the independent dynamical estimate or on the stellar population synthesis modelling. We note that the current statistical uncertainties for mass-to-light ratios derived by both dynamical and stellar population synthesis (SPS) techniques are substantial ($\Delta \log(M/L) \gtrsim 0.1$ dex, Bell and de Jong 2001; Bell et al. 2003; Cappellari et al. 2006; Zibetti et al. 2009; Conroy 2013). The main uncertainty, however, is systematic and is due to uncertainty in our knowledge of the IMF and its variations with galaxy properties. To facilitate comparison with $M_* - M$ relation calibrations from other studies, we will adopt the mass-to-light ratios corresponding to the Chabrier (2003) IMF as our fiducial choice, but will discuss effects of the IMF variation in Section 4.1.

Cappellari et al. (2006) present comparisons of the $I$-band mass-to-light ratios derived from dynamical analysis to those derived from the stellar population synthesis (SPS). The largest values correspond to the most massive galaxies, which have maximum SPS $M/L_I \approx 3$ for the Kroupa IMF or $M/L_I \approx 3/10^{0.05} \approx 2.7$ for the Chabrier IMF (see, e.g., Table 2 in Bernardi et al. (2010)). This is similar to the value of $M_*/L_I = 2.65$ adopted by Gonzalez et al. (2013), who have derived it using luminosity-dependent dynamical mass-to-light ratio of Cappellari et al. (2006) and averaged it over $I$-band luminosity function for galaxies with $L_I > 0.25L_{*,I}$. The average $M/L$ is dominated by $L \approx L_*$ galaxies for which dynamical mass-to-light ratios are consistent with those expected for the Chabrier IMF.

To estimate stellar masses from the luminosities measured from SDSS data for nine clusters described above, we have used relation between $M/L$
and galaxy color derived from the stellar population synthesis (SPS) models of Bell et al. (2003):
\[
\log_{10}(M_*/L_r)_{\text{pop}} = 1.097 \times (g-r) - 0.306 \quad \text{and} \quad \log_{10}(M/L)_{\text{pop}} = 0.864 \times (g-r) - 0.222.
\]
Massive cluster galaxies exhibit substantial radial color gradients. Therefore, we use color profile to convert luminosities to stellar mass at each particular radius. The projected stellar surface density profiles were thus obtained from the surface brightness profiles, \( \Sigma_M = (M/L)_{\text{pop}}(R) \times \Sigma_L(R) \), for \( r \) and \( i \) bands. The total stellar mass was obtained by integrating the profiles to infinity using the best fit three-component Sérsic model for \( \Sigma_L(R) \).

The mass-to-light ratios derived by Bell et al. (2003) correspond to the “diet Salpeter” IMF and are \( \Delta \log(M/L) \approx 0.1 \) dex above the mass-to-light ratios expected for the Chabrier IMF Bell and de Jong 2001; Bell et al. 2003; Bernardi et al. 2010). We therefore adjust the resulting stellar masses down by \( \Delta \log(M_*) \approx 0.1 \) dex. We have checked that we get very similar stellar masses for the brightest cluster galaxies if we use a constant value \( M_*/L_r = 3.0 \) which is predicted for the Chabrier IMF for the typical color \( g-r \approx 0.8 \) of massive ellipticals in our sample (see the \( M/L \)-color relations in the Appendix of Zibetti et al. (2009)). We have also checked that we obtain indistinguishable stellar masses from \( r \)- and \( i \)-band luminosities. We will present \( r \)-band derived stellar masses in the remainder of this paper.

Overall, there is a reasonably good agreement between our derived BCG stellar masses and those derived by G13, although stellar masses measured by G13 appear to be somewhat higher for low mass clusters, \( M_{500} \approx 10^{14} M_\odot \). It is not clear whether this difference is systematic given a small number of objects in the two samples. The background level is comparable in both analyses and thus difference in surface density sensitivity unlikely plays a role. Nevertheless, the outer profiles of BCGs in the G13 sample are typically traced to radii \( \approx 300 \) kpc, compared to a typical outer radii of \( \approx 100-200 \) kpc for our clusters. This difference can be due to a higher amplitude of the outer surface density components in their systems, as this amplitude varies from cluster to cluster. Significant contribution to the total stellar mass of BCGs comes from extrapolation of this outer component to infinity and thus even modest differences in amplitude for some clusters can lead to some difference in the derived total stellar mass. We have compared the masses measured in the two studies within a fixed aperture of 50 kpc, not affected by outer regions and profile extrapolations. The masses measured within this aperture are in good agreement, which implies that there are no systematic differences due to different mass-to-light ratios. In the reminder of this paper we will use both G13 and our data jointly in most of the analyses.

### STELLAR CONTENT OF HIGH MASS HALOS

In this section we explore the connection between bulk properties of massive halos, such as their mass and radius, and stellar masses and sizes of galaxies they host. We will also consider how these properties of high mass halos are related to the corresponding properties of smaller, galaxy-scale halos. Before we can consider such relation, we need to identify appropriate counterparts to the central galaxies in galaxy-sized halos among cluster galaxies.

Low and high mass halos differ qualitatively in the way stellar mass is distributed. In galaxy-sized

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\(^6\)Only in two clusters, Abell 2029 and Abell 85, we trace profile significantly beyond 200 kpc, out to 270 and 340 kpc, respectively.
halos most of the stellar mass is concentrated in the central galaxy, while in cluster-sized halos significant fraction of stars is in satellite galaxies. Nevertheless, brightest cluster galaxies occupy a special place among galaxies in cluster-sized halos. First, in most X-ray clusters BCGs are located close to the center of cluster halo (e.g., Skibba et al. 2011). Second, as we discussed in Section 2 above, distribution of stars associated with BCGs extends to hundreds of kpc—i.e., a significant fraction of the cluster virial radius. The outer regions of BCGs are often called the intracluster light and are interpreted as a separate component forming via mergers and tidal disruption of satellite galaxies.

Although the stars in the outskirts of the BCGs may indeed have a different origin than stars in the inner regions, Fig. 1 shows that surface density profiles of BCGs extend smoothly to the largest reliably probed radii. Although profiles do have weak features, which require multiple components for accurate modelling, these features are subtle and occur at different radii in different objects. The profiles do not show clearly distinct components with very different profiles, which can justify clean separation similar, for example, to the bulge–disk decomposition in late type galaxies. Thus, in practice, the outer component of BCGs cannot be cleanly and reliably separated based on the surface density profiles alone. Such decomposition would also create questions about comparisons of stellar masses derived for BCGs and stellar masses of smaller mass galaxies, for which no such separation is done when their luminosity and stellar mass are estimated. For example, Bernardi et al. (2013) fit single Sérsic component to all SDSS galaxies and derive stellar mass function that does not contain any features which would be associated with emergence of a distinct ICL component unique only to cluster halos. As we have shown above in Section 2.2 (see Fig. 2), such single Sérsic component fits recover luminosity of BCGs similar on average to that recovered using a more detailed with with three Sérsic components. Finally, removal of the outer component creates problems for comparisons with theoretical models, as this would require detailed modelling of the BCG profiles to closely mimic the observational component decomposition procedure. This is often difficult or impossible in practice.

Given these considerations, we will not attempt to separate the outer component of BCGs in our analysis below. We also advocate defining stellar mass in well specified apertures fixed in physical scale or at a fixed fraction of virial radius and provide such mass measurements for our BCGs in the Appendix B.

**BCG Stellar Mass—Halo Mass Relation**

Figure 4 shows relation between stellar mass of the brightest cluster galaxies and cluster mass, $M_{500}$, for the nine clusters analyzed in this paper, while squares show BCGs from the recent analysis of Gonzalez et al. (2013). The orange band shows the best fit power law relation and its 1σ uncertainties in normalization and slope (see Table 2). The solid and dotted lines show relation derived using the abundance matching approach with and without scatter (i.e., assuming a scatter of $\Delta \log (M_\ast) = 0.2$, 0.4 dex in stellar mass at fixed halo mass) using stellar mass function measured by Bernardi et al. (2013). The long and short dashed curves show relations derived by Moster et al. (2013) and Behroozi et al. (2013b) using abundance matching approach, but using different stellar mass functions. The total halo masses presented in the relations from the latter two studies were converted to $M_{500}$ using average halo mass-concentration relation.
onto the vertical direction using the final best fit slope. The results of this and other fits are summarized in Table 2. The best fit slope of the relation is similar to the slope $0.33 \pm 0.06$ of the relation of $K$-band BCG luminosity and $M_{200}$ found by Lin and Mohr (2004) for clusters in the same mass range. Our measured scatter of $\Delta \log M_{\ast} \approx 0.17$ dex is somewhat larger than the $\approx 34\%$ fractional scatter found by these authors, but the difference is not very significant compared to uncertainty of scatter. Note that the scatter we measure at the cluster mass scale is comparable to the scatter estimated at the galaxy mass scale by More et al. (2011) in their analysis of satellite kinematics.

In addition to observational points, Fig. 4 shows the $M_{\ast}-M_{200}$ relations expected from the abundance matching ansatz, in which relation between total halo mass, $M$, and stellar mass of galaxies they host, $M_{\ast}$, is established implicitly by matching cumulative stellar and halo mass functions. In the simplest implementation of this model, the cumulative abundances are matched directly, assuming no scatter in the relation between stellar and halo masses: $n(>M_{\ast}) = n(>M)$. However, it is straightforward to include scatter in this approach (see Appendix A). Figure 4 shows that relations predicted by the AM ansatz in recent studies$^7$ of Moster et al. (2013) and Behroozi et al. (2013b), shown by the long and short dashed lines, underestimate stellar masses at a given halo mass for such massive galaxies by a factor of up to $\gtrsim 5$. The reason for this discrepancy is significant underestimate of luminosities and stellar masses for high-mass galaxies in the stellar mass functions adopted to derive these relations, as was shown recently by Bernardi et al. (2013) and as we discussed above in Section 2.2.

The solid and dotted lines in Fig. 4 show results of abundance matching with and without scatter in the $M_{\ast}-M$ relation, as described in the Appendix, using the Bernardi et al. (2013) stellar mass function derived from the luminosity functions with corrected photometry for the luminous galaxies. As could be expected from the good agreement between the Bernardi et al. (2013) luminosities and the luminosities measured in our study (see Fig. 2), these abundance matching results are in considerably better agreement with observed $M_{\ast}-M$ relation for the brightest cluster galaxies.

Radial Profiles and Sizes of the BCG Galaxies

Results in the previous section show that stellar masses of BCG galaxies correlate with the total stellar mass of their parent halo with scatter comparable to that for the MW-sized galaxies. Here we examine whether characteristic size of stellar distribution of BCGs correlates with halo virial radius. It is well known that galaxies exhibit a correlation between their half-mass radii and stellar masses (e.g., Bernardi et al. (2014), and references therein). The

$^7$These studies present relation for the halo masses defined using overdensity of $200\rho_{\text{crit}}$ and virial overdensity, respectively. We have converted these masses to the overdensity of $500\rho_{\text{crit}}$ assuming NFW profile form and $c-M_{\text{crit}}$ relation predicted by the model of Bullock et al. (2001) but a constant minimum “floor” of concentration $c_{\text{crit}} = 3.5$ at large masses (Zhao et al. 2003).
relation is complicated, however, and cannot be described by a single power law across a wide range of masses.

Given that there is abundant evidence that stellar masses of galaxies correlate with total masses of their host halos, the correlation of sizes with halo mass and virial radius is also expected. What is remarkable, however, is that the resulting relation between galaxy sizes and virial radii of their host halos is close to linear over the entire range of stellar masses (Kravtsov 2013). This indicates that sizes of galaxies are set by properties of baryons tightly connected to properties of dark matter, while the complicated size-stellar mass relation is simply a reflection of the complicated non-linear $M_\ast - M_{200}$ relation resulting from a complicated interplay between star formation and feedback during galaxy evolution. Here we examine how sizes of BCGs, as galaxies representing the most extreme massive end of galaxies, fit into this picture.

Figure 5 shows the relation between three dimensional half-mass radius of stellar distribution and virial radius of their halo, $R_{200}$. The latter is estimated using $M_\ast - M_{200}$ relation derived from abundance matching and $R_{200}$ calculated from $M_{200}$ for all galaxies, except for BCGs for which we use $R_{200} \approx 1.67R_{500}$ appropriate for NFW profile with a typical concentration for cluster halos. The abundance matching is carried out using the Bernardi et al. (2013) SMF with $\Delta \log M_\ast = 0.2$ dex scatter in $M_\ast$ at a fixed $M_{200}$, as described above (see also Appendix A). The sample of late type and early type galaxies shown in the Fig. 5 is identical to that presented in Kravtsov (2013). Here we also add half-mass radii of the BCGs in the nine clusters analyzed in this paper. To estimate the half mass radii we use the three-component Sérsic fit to the stellar surface density profiles and measure the projected radius containing half of the total stellar mass measured by extrapolating the best fit three-component fit to infinity. The projected effective radius is then converted into the 3D half-mass radius using $r_{1/2} = 1.34R_e$, the expression accurate for spheroidal systems described by the Sérsic profile with a wide range of the Sérsic index values (see Eq. (21) in Lima Neto et al. (1999)). The 3D half-mass radii measured in this way are shown in Fig. 5 as a function of $R_{200}$ as open circles.

We can see that the half-mass radii of BCGs lie above the average $r_{1/2} \approx 0.015 R_{200}$ relation but are still within the scatter exhibited by smaller mass galaxies and scatter expected from the distribution of spins if sizes are set by specific angular momentum shown by the dotted lines. However, one should note that the actual half mass radii could be larger if the extrapolation of the triple-Sérsic profile underestimates stellar mass profile beyond the largest radii of our measurements. As we discuss in Section 2.1, such underestimate should have an effect of $\lesssim 30\%$ on the total BCG stellar mass. The half-mass radius can, nevertheless, be significantly affected. One should therefore view the open circles in Fig. 5 as lower limits.

Recently, Huang et al. (2013a) have used three-component Sérsic fits for a sample of nearby massive elliptical galaxies and showed that the relation between half mass radii and stellar masses of the inner two components resembles that size-stellar mass relation of $z \approx 1$ compact red galaxies. They proposed an evolutionary scenario in which the inner regions of massive ellipticals form by dissipative collapse of baryons at high $z$, while outer regions form by accretion and mergers at later epochs. We show the half mass radii and stellar masses of the inner plus middle Sérsic components for the nine BCGs analyzed in this study by solid red circles in Fig. 5. As we noted above, separation into separate components based on the surface density profiles is likely to be noisy. Nevertheless, the figure shows that the sizes and stellar masses of the combined two inner Sérsic components are scattered around the average $r_{1/2} \approx 0.015 R_{200}$ relation and are thus consistent with the size–virial radius correlation of smaller mass galaxies. This means that the inner regions of BCGs could indeed form via processes similar to those shaping structure of smaller mass galaxies. This can be seen even more clearly if we compare stellar surface density profiles of BCGs with those of smaller mass galaxies.

Figure 6 shows the normalized surface density profiles of nine BCGs in our sample compared to the median profile of massive early type (Sérsic index $n > 2.5$) SDSS galaxies from Szomoru et al. (2013) and late type galaxies from the THINGS and LITTLE THINGS samples derived in Kravtsov (2013). The radii are normalized by the radius $r_n = 0.015 R_{200}$, while the surface densities of galaxies are normalized by $\Sigma_n = M_\ast / (\pi R_{\text{eff}}^2)$, where $R_{\text{eff}}$ is the half mass radius of stellar distribution. For the BCG galaxies, $M_\ast$ and $R_{\text{eff}}$ are the stellar mass and half mass radius of the inner and middle Sérsic components. The error bars around thick red lines show rms dispersion around the median. The figure shows that the inner regions of the BCGs have profiles that are scaled versions of the profiles of smaller mass early type galaxies. Remarkably, at $R \gtrsim r_n$ profiles of all early and late type galaxies have similar shape (see also Kravtsov 2013; Fang et al. 2013).

Results presented in these figures show a striking similarity between the inner regions of all elliptical galaxies. Remarkably, the sizes of late type, early type and the inner regions of BCG galaxies all corresponds to a similar fraction of the virial radius, which indicates that sizes of all galaxies may be set by a similar mechanism. Indeed, as discussed in Kravtsov (2013),
Fig. 6. (Color online) Normalized surface mass density profiles of nine BCGs in our sample (thin red lines) compared to the median profile of massive early type (Sérsic index $n > 2.5$) SDSS galaxies from Szomoru et al. (2013) and late type galaxies from the THINGS and LITTLE THINGS samples (blue, dashed line, see Kravtsov (2013) for details). Profiles are normalized by the radius $r_n = 0.015R_{200}$ which approximately corresponds to the half mass radius of stellar distribution. Here for smaller galaxies $R_{200}$ is obtained using the abundance matching ansatz from galaxy’s $M_*$, while for BCGs we use $R_{200} = 1.67R_{500}$, where $R_{500}$ is measured from X-ray data. The surface densities of galaxies are normalized by $\Sigma_0 = M_*/(\pi R_{\text{eff}})^2$, where $R_{\text{eff}}$ is the half mass radius of stellar distribution. For the BCG galaxies $M_*$ and $R_{\text{eff}}$ are the stellar mass and half mass radius of the inner and middle Sérsic components (see Section 3.2 for details). The error bars around thick red lines show rms dispersion around the median. The figure shows that the inner regions of the BCGs have profiles that are scaled versions of the profiles of smaller mass early type galaxies. Remarkably, at $R > r_n$ profiles of all late and early type galaxies have similar shape.

Fig. 7. (Color online) Total stellar mass within $R_{500}$ versus total halo mass, $M_{500}$. Circles show the clusters analyzed in this paper, while squares show clusters from the recent analysis of Gonzalez et al. (2013). The orange band shows best fit power law relation; its width reflects 1σ uncertainties in normalization and slope. The dot-dashed line shows results of the HOD modelling of Leauthaud et al. (2012b). Blue solid line shows relation calculated using halos and subhalos from the Bolshoi simulations with stellar masses assigned using the mean relation derived using abundance matching without scatter.

The average $r_{1/2} \approx 0.015R_{200}$ is consistent with expectations of the Mo et al. (1998) model in the case when the specific angular momentum of baryons is similar to that of dark matter. The BCGs do have the outer extended envelope that likely forms by mergers and tidal stripping of satellite galaxies (e.g., Murante et al. 2007; Conroy et al. 2007a; Purcell et al. 2007; Puchwein et al. 2010; Feldmann et al. 2010; Watson et al. 2012) and can thus be significantly larger than the size defined by the angular momentum limit. Our results thus are consistent with scenario, in which the inner stellar distribution of BCGs is set early via dissipative processes, while the outer regions are built up over longer period of time by mergers and accretion. The sizes of BCGs are correlated with the virial radii of their parent cluster and lie on the extension of the corresponding relation for smaller mass galaxies.

**Total Stellar Mass—Halo Mass Relation**

Having examined correlation of properties of the BCG with cluster mass and virial radius, in this section we investigate correlation of the total stellar mass of clusters with their total mass. Figure 7 shows the total stellar mass within $R_{500}$ as a function of $M_{500}$. It is clear that this relation is steeper and tighter than relation for stellar mass of the BCG. The best fit slope is $0.59 \pm 0.08$, while the scatter in total stellar mass at a fixed $M_{500}$ is only $0.11 \pm 0.02$ (see Table 2). The tightness of this relation has been noted by Andreon (2012), who quoted 90% upper limit on scatter of $\Delta \log M_* < 0.06$ dex and argued that total stellar mass can be a good total mass proxy rivaling X-ray proxies, such as gas mass and $Y_X$. Using a larger sample, we find a larger scatter of $\approx 29\%$, comparable to scatter of total X-ray luminosity (without core excision) or richness (e.g., Rykoff et al. 2012) at a fixed mass, but several times larger than scatter in gas mass and $Y_X$ (e.g., Kravtsov et al. 2006; Nagai et al. 2007). Our best fit slope is also significantly
stellar mass—halo mass relation

Our results are closer to those of Lin et al. (2004), who found that the total $K$-band luminosity–$M_{500}$ relation has slope of $0.69 \pm 0.04$ and scatter of $\approx 32\%$. Our fit is also close to the best fit relation derived by Lin et al. (2012) for a sample of 94 clusters at $0 \lesssim z \lesssim 0.6$ for which stellar masses were estimated using IR data from 2MASS survey and the WISE satellite, while total masses were estimated using X-ray mass proxies. In fact, the best fit relation for this sample is a good fit to the nine SDSS clusters analyzed in this study, although normalization is somewhat lower than the best fit for the combined sample of 21 clusters. Lin et al. (2012) found that the normalization of the relation does not evolve with redshift within uncertainties (see also van der Burg et al. 2014) and thus comparison of their results at higher $z$ to our results at $z \ll 0.1$ is justified. The scatter of $M_{\ast, \text{tot}}$ at a fixed $M_{500}$ in their sample is $0.12 \pm 0.01$ in good agreement with our results. The $M_{\ast, \text{tot}} - M_{500}$ relation derived by Leauthaud et al. (2012b), shown by the dot-dashed line in Fig. 7 based on the HOD analysis of the COSMOS data at $z \approx 0.37$ is somewhat steeper than the best fit of Lin et al. (2012) and our best fit relation.

The solid line in Fig. 7 shows the relation calculated using halos and subhalos from the Bolshoi simulation of WMAP compatible cosmology (Klypin et al. 2011) with stellar masses assigned using the mean relation derived from the abundance matching without scatter. Note that for $M_{\ast} - M$ relation of central halo galaxies we use an analytic abundance matching model described in the Appendix A, based on the observed SMF, theoretical halo mass function, and parametrization of the fraction of subhalos as a function of halo mass. However, for the total stellar masses of halos, we need to predict subhalo mass functions in host halos of different mass. This can be done either via a halo model or using halo + subhalo sample extracted from an actual simulation. Here we choose the latter approach and use the halo catalogs of Behroozi et al. (2013b).8

We use the same $M_{\ast} - M$ relation at $z = 0$ derived analytically (see Appendix A) to assign stellar masses for the central galaxies of both host halos and subhalos (i.e., halos located within $R_{200}$ of a more massive halo). For host halos we use their current $z = 0$ total mass, $M = M_{200}$. To assign stellar mass for subhalos we assume that $M$ is the maximum mass they ever had during their evolution, which was derived from their mass accretion history. This choice is motivated by the comparisons of abundance matching predictions with observed galaxy clustering (Reddick et al. 2013). Having assigned stellar masses in this way, we then compute total stellar masses of the isolated halos as a sum of stellar masses of all subhalos within $R_{200}$ of the center, including stellar mass assigned to the main halo itself. The latter corresponds to the stellar mass of the central halo galaxy.

The relation predicted by such AM ansatz has slope similar to our best fit slope for the observed clusters, but normalization lower by $\approx 30\% - 50\%$. The low normalization may be due to several different reasons. The stellar mass–halo mass relation for subhalos may have a higher normalization than normalization for central galaxies. For example, Watson and Conroy (2013) find that for a given mass, subhalos host galaxies with 10% larger stellar mass compared to host halos of the same mass. Simulation also misses halos and subhalos below resolution limit. For the Bolshoi simulation the overall mass resolution limit for halos is $\approx 2 - 3 \times 10^{10} h^{-1} M_\odot$, but this limit is larger within $R_{500}$ of $0.6 R_{200}$ of massive halos due to enhanced tidal disruption in these regions. This incompleteness can account for another $5\% - 10\%$ of stellar mass. A small difference may also exist between observed masses of clusters and masses assigned via abundance matching, because AM is based on halo mass function calibrated using dissipationless simulations. In simulations with hydrodynamics and galaxy formation $M_{500}$ may be $\approx 5\%$ smaller than in dissipationless simulations Cui et al. 2012; Martizzi et al. 2013; Cusworth et al. 2014), which would shift the predicted relation left by this amount. These effects can account for a significant fraction of the difference. Despite the discrepancy in normalization, the similarity in slope indicates that overall subhalo mass function and its scaling with host halo mass behave similarly to the real galaxies in clusters.

Figure 8 shows relation between stellar mass in satellite galaxies (i.e., the total mass minus the BCG mass) as a function of $M_{500}$. This relation is steeper yet (slope of $0.75 \pm 0.09$) and has scatter of $0.10$ dex, comparable to the $M_{\ast, \text{tot}} - M_{500}$ relation. Although $M_{\ast, \text{sat}} - M_{500}$ relation has the slope closest to unity, it is still somewhat shallower than linear scaling. The HOD estimate of Leauthaud et al. (2012b), on the other hand, exhibits close to linear scaling (see also Skibba et al. 2007). Its normalization, however, is close to the normalization of our best fit relation.

The results presented above show that the total stellar mass in cluster galaxies correlates with total cluster mass with a scatter of $\approx 0.1$ dex, comparable to the scatter in richness indicator $\lambda$ (Rykoff et al. 2012). Our results show that the low scatter of the $M_{\ast, \text{tot}} - M_{500}$ relation is due to low scatter of

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8Available at http://hipacc.ucsc.edu/Bolshoi/MergerTrees.html.
Abundance matching: w/o scatter (using B + 13 SMF)

HOD modelling: Leauthaud + 12

Observations (M500 from X-ray):
- this work
- Gonzalez + 13
- best fit

Fig. 8. (Color online) As in Fig. 7, but for the stellar mass in satellite galaxies within R500.

Fig. 9. (Color online) Fraction of the stellar mass in BCG relative to the total stellar mass within r500. Circles show the clusters analyzed in this paper, while squares show clusters from the recent analysis of Gonzalez et al. (2013). Blue dashed and solid lines show the corresponding fraction derived for halos in the Bolshoi simulation, for which stellar masses were assigned using stellar mass–halo mass relation derived using abundance matching ansatz assuming no scatter and scatter of 0.2 dex, respectively. The dotted lines show rms scatter around the solid line; the last three bins contain only one halo in the Bolshoi catalog and the rms is not defined.

EFFICIENCY OF STAR FORMATION AS A FUNCTION OF HALO MASS

Having quantified the stellar mass–halo mass relation on the cluster mass scale, we will now examine how this relation and the corresponding stellar fraction compare to observational results at smaller masses. Stellar mass fraction quantifies the efficiency with which halos convert their baryons into stars. Comparing constraints on cluster and galaxy scales can therefore give us insights into how star formation efficiency varies from galaxy-sized halos to the largest mass halos in the universe.

Figure 10 shows the stellar mass–halo mass relation for a wide range of halo masses and compares results at the high mass end to other observational estimates of this relation at smaller masses, such as weak lensing (Mandelbaum et al. 2006; Reyes et al. 2012; Hudson et al. 2013) and satellite kinematics (More et al. 2011; the earlier results by Conroy et al. 2007b are consistent with these results and are not shown). As before, we assume that BCGs in clusters correspond to the central halo galaxy. To compare results of different studies we have converted all halo masses to the common definition, M200—the mass within the radius enclosing overdensity of 200 times the critical density of the universe. We omit error bars for most data sets for clarity, but note that they are typically comparable to the symbol size, except at small masses where error in mass in weak lensing is substantial. Note that relations inferred from weak lensing stacking and satellite kinematics are statistical in nature and provide average halo mass at a given stellar mass. Nevertheless, in some of the studies the authors apply a correction to infer the true Ms–M relation. Such corrections are, however, uncertain because scatter in the relation is not well known. We therefore also plot abundance matching predictions with scatter for both ⟨Ms⟩–M200 and Ms–⟨M200⟩ relations to show the potential difference.

Figure 10 shows that galaxies follow a well defined relation from the smallest probed masses to the BCGs in the most massive clusters. In particular, the BCGs in clusters studied in this paper smoothly extend the mean relation derived for smaller mass galaxies via stacked weak lensing analyses and satellite kinematics. The relation derived under the abundance matching approach using the Bernardi et al. (2013) SMF at the high mass end is in reasonable agreement with
the well known peak in stellar fraction at the bar on budget stars. Figure 11 shows what fraction of the critical density of the universe. The BCG galaxies in the sample studied in this paper and in the sample of Gonzalez et al. (2013) are shown by red crosses; cluster masses are converted from $M_{200}$ to $M_{200}$ using the concentration–mass relation. Red and blue circles show the mean relations measured using stacked weak lensing signal for early and late type galaxies (Mandelbaum et al. 2006). Magenta triangles show the mean relation derived using stacked satellite kinematics (More et al. 2011). The solid and dotted lines show relation derived using the abundance matching approach with and without scatter (i.e., assuming a scatter of 0.2 dex and zero in stellar mass at fixed halo mass) using stellar mass function measured by Bernardi et al. (2013). Note that this relation is much steeper at the high mass end than previously derived relations using this approach (Moster et al. 2013; Behroozi et al. 2013b; see Appendix A) with different stellar mass functions. All stellar masses shown in this figure were computed assuming Chabrier IMF.

Figure 11 shows the corresponding plot of the stellar mass fraction as a function of halo mass. The stellar mass fraction is normalized by the universal baryon fraction $\Omega_b/\Omega_m \approx 0.16$ (Hinshaw et al. 2013), to gauge more conveniently what fraction of the baryon budget is in stars. Figure 11 shows the well known peak in stellar fraction at $M_{200} \approx 10^{12} M_\odot$ and a steady decrease at both low and high masses. The stellar mass fraction in central galaxies in $M_{200} \approx 10^{14} M_\odot$ halos is roughly 5–6 times lower than at the peak. Note that although this decrease is substantial, it is considerably smaller than the decrease implied by the previously derived $M_* - M_{200}$ relations (Moster et al. 2013; Behroozi et al. 2013b), which predicted stellar mass $\gtrsim 20$ lower than the peak at cluster masses. This shows that suppression of stellar masses in central cluster galaxies is milder than previously thought.

The overall efficiency of star formation in cluster halos can be represented by the total stellar mass fraction in all cluster galaxies, including the BCG and satellite galaxies, shown in Fig. 12. This figure shows the total stellar fractions in the observational cluster sample and expected from the abundance matching models. For the latter we use the $M_* - M_{200}$ relation derived using the abundance matching and the Bernardi et al. (2013) SMF to assign stellar masses to halos and subhalos in the Bolshoi simulation, as described above in Section 3.3.

Figure 12 shows that total stellar fractions derived by abundance matching are in reasonable agreement with observations. In contrast to the mass fraction in the central galaxy, the total stellar fraction is a weak function of halo mass decreasing only by a factor of three when total halo mass changes by more than two orders of magnitude (see also Leauthaud et al. 2012a, 2012b). This shows that the overall efficiency of star formation per unit mass in massive halos is only a factor of $\sim 3$–6 smaller than in the $M_{200} \sim 10^{12} M_\odot$, in which star formation efficiency reaches its peak. The key difference between $M \approx 10^{12} M_\odot$ and cluster
halos is that the former form most of their stars in the central galaxy, while a large fraction of stellar mass in cluster halos is contributed by satellite galaxies (see Fig. 9). Also, a significant fraction of stellar mass in the central galaxy in clusters is contributed by its extended outer component, while in the MW-sized galaxies stellar halo, which could be considered to be an equivalent of such component, contributes only \( \sim 1-2\% \) of stellar mass (e.g., Purcell et al. 2007).

**Effects of IMF**

Recently, several observational studies have inferred that stellar IMF of early type galaxies becomes increasingly “bottom–heavy” with increasing velocity dispersion and stellar mass. These studies used a variety of techniques, from indirect dynamical constraints on the mass–to–light ratios of stars (Grillo et al. 2009; Grillo and Gobat 2010; Treu et al. 2010; Auger et al. 2010; Sonnerfeld et al. 2012; Dutton et al. 2011, 2012, 2013; Cappellari et al. 2013; Conroy et al. 2013) to direct probes of abundance of dwarf stars with \( m \approx 0.1–0.2 \, M_\odot \) relative to abundance of \( m \approx 1 \, M_\odot \) stars using unique spectral features of dwarf stars (van Dokkum and Conroy 2010; Spiniello et al. 2012; Conroy and van Dokkum 2012). Currently, observational constraints probe only the inner regions of galaxies (\( \lesssim R_e \), where \( R_e \) is effective radius of galaxy surface brightness profile) and IMF may vary with galaxy radius. Nevertheless, if we assume that results for the inner regions are applicable for the entire stellar populations of these galaxies, we can obtain an upper limit on the possible effect of IMF variation on the stellar content of clusters.

To model effect of such variation, we adopt recent calibration of the trend of the stellar mass–to–light ratio with galaxy velocity dispersion for a sample of compact early type galaxies by Conroy et al. (2013), see their Fig. 3. The trend is defined with respect to the fiducial Milky Way Chabrier IMF and parametrized as:

\[
\log_{10} \left( \frac{(M/L)_*}{(M/L)_{\text{Chabrier}}} \right) = a + b \log_{10} \left( \frac{\sigma}{130 \, \text{km s}^{-1}} \right),
\]

where \( \sigma \) is velocity dispersion within the SDSS fiber and \( a = 0.13 \) and \( b = 0.9 \) approximate the trend in Fig. 10 of Conroy et al. (2013). A similar but somewhat weaker trend was also derived recently using dynamical modelling by Cappellari et al. (2013). We adopt a stronger trend of Conroy et al. (2013) here in the spirit of estimating the upper limit on the effect. We use the relation between the central velocity dispersion and stellar mass for early type galaxies given by Eq. (5) of Cappellari et al. (2013) and associated parameters to convert velocity dispersion to stellar mass and obtain the corresponding variation of the mass–to–light ratio as a function of stellar mass for early type galaxies.

To evaluate the effect of IMF variation on the stellar mass function, we use the parametrizations of the SMFs for late and early type galaxies provided in Table 3 of Bernardi et al. (2013). Given that systematic trend of IMF is deduced for early type galaxies, we only correct the combined SMF of lenticular and elliptical galaxies by the mass–to–light ratio dependence as a function of stellar mass, derived as described above, while leaving the SMF of late type galaxies intact. We then construct the combined SMF as a sum of the early type galaxy SMF corrected for IMF variation and the uncorrected SMF of late type galaxies. We then re-derive the stellar mass–halo mass relation using abundance matching with this new SMF. The results for the fraction of stellar mass in the central galaxy and for the total stellar mass fraction within \( R_{200} \) are shown in Figs. 13 and 14.

As expected, the increase of stellar mass–to–light ratio with increasing stellar mass for early type galaxies results in steeper \( M_* - M_h \) relation and, corre-
spondingly, shallower dependence of $f_{\ast,\text{cen}}$ on halo mass. The stellar mass fraction of the central galaxies increases by a factor of $\sim 1.5 - 2$. In this case, for $M_{200} \approx 10^{14} M_\odot$ halos stellar fraction of the central galaxy is only a factor of $\sim 3 - 4$ smaller than the peak fraction at $M_{200} = 10^{12} M_\odot$. Likewise, the total stellar fraction within $R_{200}$ has increased by a factor of $\sim 1.6 - 1.7$ in the cluster halos or by $\sim 0.04 - 0.06$ in absolute values in units of $\Omega_b/\Omega_m$. This increase is non-negligible for the total baryon census in clusters and can, in principle, explain part of the “baryon bias”—the difference between the estimated baryon content of clusters and the universal fraction (see, e.g., G13). It is worth keeping in mind, however, that the effect of IMF variation predicted by our model is an upper limit and the actual effect can be significantly smaller.

The main effect of varying IMF is to make the

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**Table 3.** Parameters of best fit $M_\ast - M$ parametrization at $z \lesssim 0.1$

| Mass definition   | $\log_{10}(M_\ast/M_\odot)$ | $\log_{10} \epsilon$ | $\alpha$ | $\delta$ | $\gamma$ |
|-------------------|-------------------------------|------------------------|--------|--------|--------|
| $M_{200\text{c}}$ (no scatter) | 11.39                          | -1.618                 | -1.795 | 4.345  | 0.619  |
| $M_{200\text{c}}$ (with scatter) | 11.35                          | -1.642                 | -1.779 | 4.394  | 0.547  |
| $M_{500\text{c}}$ (no scatter) | 11.32                          | -1.527                 | -1.856 | 4.376  | 0.644  |
| $M_{500\text{c}}$ (with scatter) | 11.28                          | -1.556                 | -1.835 | 4.437  | 0.567  |
| $M_{200\text{m}}$ (no scatter) | 11.45                          | -1.702                 | -1.736 | 4.273  | 0.613  |
| $M_{200\text{m}}$ (with scatter) | 11.41                          | -1.720                 | -1.727 | 4.305  | 0.544  |
| $M_{\text{vir}}$ (no scatter) | 11.43                          | -1.663                 | -1.750 | 4.290  | 0.595  |
| $M_{\text{vir}}$ (with scatter) | 11.39                          | -1.685                 | -1.740 | 4.335  | 0.531  |

---

Fig. 13. (Color online) The stellar mass fraction of the central galaxy in units of the universal baryon fraction within radius $R_{200}$ as a function of total halo mass $M_{200}$. The dashed is prediction of the abundance matching model without scatter using the SMF of Bernardi et al. (2013) with fixed Chabrier IMF. The solid line shows the abundance matching prediction using the SMF, in which stellar masses of early type galaxies have been corrected for the varying IMF, as described in the text.

Fig. 14. (Color online) Total stellar fraction within radius $R_{200}$. The dashed line shows prediction of the abundance matching model without scatter using the SMF of Bernardi et al. (2013) with fixed Chabrier IMF. The solid line shows the abundance matching prediction using the SMF, in which stellar masses of early type galaxies have been corrected for the varying IMF, as described in the text. Because in the latter case IMF becomes progressively more bottom-heavy with increasing galaxy mass, the total stellar fraction exhibits a weaker dependence on halo mass compared to the stellar fraction inferred assuming fixed IMF.
overall slope of the $f_{*,101} - M_{200}$ relation considerably shallower. In this case, the total stellar fraction in units of the universal fraction varies between the peak value of $\approx 0.35$ at $M_{200} \approx 10^{12} M_\odot$ and $\approx 0.1$ at $M_{200} \approx 10^{15} M_\odot$. A similar conclusion was reached in a recent study by McGee et al. (2013), although these authors have studied models in which IMF variations were even stronger than considered here.

**DISCUSSION**

We have presented measurements of stellar mass for galaxies in nine clusters using SDSS data, using new photometry based on careful modelling of large-scale background and extended surface brightness profiles of massive galaxies. We show that stellar masses of BCGs derived in our analysis are a factor of $\approx 2-4$ larger than the masses derived from the SDSS cmodel magnitudes, but are close to the stellar masses derived by the photometric analysis used in recent new measurement of the stellar mass function of galaxies by Bernardi et al. (2013).

Combining stellar mass measurements with the total masses measured using X-ray Chandra data for these clusters and with similar measurements for 12 clusters from Gonzalez et al. (2013) allows us to study stellar mass–halo mass relation for the highest mass halos at $z \approx 0$. We show that the relation between BCG stellar mass and total cluster mass has significantly higher normalization and steeper slope than in the previous observational studies (see also discussion in Section 5.1 below). Our results thus indicate that stellar and AGN feedback parameters in semi-analytic models and simulations, which were tuned to reproduce previous calibrations of the $M_* - M$ relation, significantly overestimate the effects of feedback and over suppress star formation in massive halos.

Our results also indicate that high mass halos are only modestly less efficient in converting their baryons into stars than halos hosting $L_*$ galaxies. In particular, the total stellar fraction in cluster halos is a factor of $\approx 3-6$ smaller than the peak fraction in $M \approx 10^{12} M_\odot$ halos, if the IMF is universal, and could be only $\approx 1.5-3$ times smaller than the peak value, if the IMF in early type galaxies is bottom-heavy, as indicated by recent observational analyses.

This may seem surprising given that there are many processes that could be invoked to suppress star formation in such massive halos. For example, progenitors of these halos spend a significant fraction of time in the “hot accretion” regime, which is thought to suppress direct accretion of cold gas onto galaxies. Nevertheless, a significant fraction of mass that builds up group and cluster halos is contributed by $\approx 10^{12}-10^{13} M_\odot$ halos, i.e., halo masses close to the peak of star formation efficiency. As host halo mass increases, the dynamical friction time for orbital decay of such accreted galaxies increases as well. Thus, although star formation in the BCG galaxy is suppressed, satellites contribute increasingly larger fraction of the total stellar mass fraction in halos of larger mass.

The satellite galaxies that do merge or get tidally disrupted contribute substantial stellar mass to the outer regions of the BCG galaxies (e.g., Conroy et al. 2007a). For example, the model of Behroozi et al. (2013b) predicts that disrupted satellites deposit up to $\approx 10^{12} M_\odot$ of stellar mass to the ICL in $M \approx 10^{14} M_\odot$ clusters, a factor of $\approx 4-5$ larger than the stellar mass of the BCGs in halos of that mass (see their Fig. 9). Thus, the total stellar mass of the BCG and ICL predicted in their model is in reasonable agreement with our measurement of the BCG mass that include stellar mass at large radii. This once again illustrates that the discrepancy of the BCG mass between our measurements and their model is simply due to the fact that their inference is based on observational stellar mass function that do not measure the outer profiles of BCGs properly. The stellar mass of disrupted satellites in their model thus has to be attributed to a separate ICL component rather than to the outer regions of the BCG galaxy. In other words, their model for satellite accretion and disruption actually predicts that the stellar mass associated with the central cluster galaxies is as massive as in our analysis.

Our results provide an interesting avenue for testing such models by comparing stellar mass distribution in the observed BCG galaxies and predicted by the model.

These considerations show that the fact that massive halos have stellar fractions only moderately lower than those of $\approx L_*$ galaxies, is due primarily to the hierarchical nature of structure formation and high efficiency of star formation in their progenitors that contribute the bulk of the mass.

**Comparison with Previous Studies**

Stellar mass fractions have recently been estimated in a number of studies (Lin et al. 2003, 2012; Gonzalez et al. 2007; Giodini et al. 2009; Andreon 2010, 2012; Zhang et al. 2010; Laganà et al. 2011, 2013; Leauthaud et al. 2012a, 2012b; Budzynski et al. 2014; Gonzalez et al. 2013). A detailed comparison between these studies and measurements of the total stellar fraction for the G13 clusters is presented in Section 5.5 of G13 (see their Fig. 10). The main difference between G13 and previous studies is in the inclusion of the mass in the outer regions of BCGs, which is usually missed by the standard survey photometry employed in previous measurements. For example, G13 measurements are consistent with most
other studies if stellar mass of the central galaxies is estimated within central 50 kpc only. Given that we also include stellar masses at large radii, our results are in good agreement with G13 and similar conclusion holds for comparison of our results with previous studies.

The total stellar mass fractions derived by Leauthaud et al. (2012b) using the halo modelling of the COSMOS data are the most discrepant with the results of G13. In particular, the total stellar fraction inferred by Leauthaud et al. (2012b) is almost constant (at ≈0.08–0.09 in units \( \Omega_b/\Omega_m \) for the Chabrier IMF) over the mass interval probed by cluster data. A similar conclusion was recently reached by Budzynski et al. (2014), who used optically-selected SDSS group and cluster catalog of Budzynski et al. (2012) and measured stellar fractions both using SDSS cmodel photometry of cluster galaxies and including all of the light measured by stacking cluster images. For Chabrier IMF they derive an approximately constant total stellar fraction of 0.08 in units \( \Omega_b/\Omega_m \) for the interval \( M_{500} \approx 10^{14} \)–\( 10^{15} \) \( M_\odot \). The total stellar fractions of G13 and our clusters, however, systematically decrease with increasing cluster mass.

We compare stellar fractions measured for our clusters along with measurements of G13 to the stellar fractions contributed by the central galaxy, satellite galaxies, and the total fraction (central + satellites) with the HOD results of Leauthaud et al. (2012b) in Fig. 15. The figure also shows results of the abundance matching analyses presented in this study and results for central galaxies from Moster et al. (2013) and Behroozi et al. (2013b). The left panel of Fig. 15 shows that the stellar fraction of central galaxies derived by Leauthaud et al. (2012b) is close to our results at \( M_{500} \lesssim 10^{13} \) \( M_\odot \), but is significantly below direct measurements and our abundance matching results for \( M_{500} \gtrsim 10^{14} \) \( M_\odot \). At high masses their results are close to the AM results of Moster et al. (2013) and Behroozi et al. (2013b). As we discussed above, these analyses use SMFs in which the stellar masses of central galaxies were significantly underestimated (Bernardi et al. 2013) and therefore underestimate the stellar fractions of central galaxies in the high mass halos.

Comparison of stellar fractions contributed by satellite galaxies in the middle panel shows that there is reasonable agreement between results of Leauthaud et al. (2012b) and direct measurements in clusters. The main source of the difference in the total stellar fractions at \( M_{500} \approx 10^{14} \) \( M_\odot \), apparent in the right panel of Fig. 15, is thus in the masses of BCG galaxies. We find that these galaxies contribute a significant fraction of the total stellar mass. Decrease of the BCG stellar fraction with increasing halo mass is thus the source of the corresponding decrease of the total stellar fraction with increasing halo mass.

The reasons for a similar discrepancy with results of Budzynski et al. (2014) are less clear as these authors do include contribution of the extended component in their analysis of stacked images. Surprisingly,
Implications for Galaxy Formation Models and Feedback

Stellar content of group and cluster halos and the overall stellar mass function of galaxies are frequently used as a diagnostic of feedback prescriptions in models of galaxy formation. For example, stellar mass–halo mass relation is often used to tune parameters of semi-analytic models and phenomenological recipes in galaxy formation simulations. We show that normalization of this relation is a factor of $\approx 2$–4 higher than derived in previous studies and suppression of star formation in massive halos by AGN and stellar feedback is therefore considerably weaker than previously thought. Prescriptions for such feedback in semi-analytic models thus need to be revised.

Cluster formation simulations generically predict that total stellar fraction is only a weak function of cluster mass (e.g., Kravtsov et al. 2005; Puchwein et al. 2010; McCarthy et al. 2011; Planelles et al. 2013; Martizzi et al. 2013), i.e., total stellar mass scales almost linearly with cluster mass. Varying physical prescriptions for star formation changes the overall value of the total stellar fraction, but not its (in)dependence on total mass (e.g., Puchwein et al. 2010; McCarthy et al. 2011; Planelles et al. 2013). In contrast, stellar fraction in observed clusters considered in our study and by G13 show a systematic decrease of the total stellar fraction with increasing cluster mass. The reason for the difference in this case appears to be a nearly linear scaling of stellar mass of both the BCG and satellite galaxies with the total cluster mass (e.g., Puchwein et al. 2010; McCarthy et al. 2011; Planelles et al. 2013).

The discrepancy indicates that feedback and other relevant physical processes included in simulations need further improvement. At the same time, some differences may arise simply due to differences in how stellar mass is defined and measured. Therefore, care should be taken to measure stellar mass in simulation analysis mimicking observational measurement as closely as possible. The importance of mass definition is illustrated in Fig. 16, where we show comparison of stellar masses of the BCGs in observed clusters in our sample and recent simulations by Martizzi et al. (2013). These authors define the stellar masses in exactly the same way as Martizzi et al. (2013); i.e., by counting all of the stellar mass in regions around the center where 3D stellar density is $\rho_\star > 2.5 \times 10^5 M_\odot$ kpc$^{-3}$. These stellar masses are shown as red solid circles. For the G13 clusters we show (red solid squares) stellar masses measured within central 50 kpc, which approximately corresponds to an average radius defined by the above stellar density threshold condition. Corresponding open circles and squares show the total stellar masses of central galaxies and their extended halos presented in previous studies. Magenta points show predictions of simulations with AGN feedback by Martizzi et al. (2013). The solid and dotted lines show relation derived using the abundance matching approach with and without scatter using the SMF of Bernardi et al. (2013).
is at radii >50 kpc and detailed comparisons with simulations should also include comparisons of stellar mass defined within larger radii. We advocate using masses measured within specific apertures for such comparisons and provide such measurements for our BCGs for a range of apertures in Table 4 in the Appendix B.

CONCLUSIONS

In this study we investigated stellar mass—halo mass relation and corresponding efficiency of star formation for high mass halos using a sample of galaxy clusters with careful measurements of stellar and total masses. Our main results and conclusions can be summarized as follows.

1. Stellar surface density profiles of the BCGs in the nine clusters analyzed in this study are well described by three Sérsic components and extend smoothly out to ≥100–300 kpc. The cumulative stellar mass of the BCG galaxies continues to grow at the last reliably measured radius in all of the BCGs.

2. We show that the stellar surface density profiles of BCGs in the inner regions are similar to the stellar surface density profiles of lower mass elliptical galaxies and to the outer regions of late type galaxies. Sizes of BCG galaxies correlate with the virial radius of host cluster halo and smoothly extend the corresponding correlation for smaller mass galaxies.

3. We find that stellar mass of the BCGs correlates with the total cluster mass as $M_{\star, \text{BCG}} \propto M_{500}^{\alpha_{\text{BCG}}}$ with the best fit slope is $\alpha_{\text{BCG}} \approx 0.4 \pm 0.1$ and scatter of $\approx 0.1$ dex. For the stellar mass in satellite galaxies $M_{\star, \text{sat}} \propto M_{500}^{\alpha_{\text{sat}}}$, the best fit slope is $\alpha_{\text{sat}} \approx 0.8 \pm 0.1$ and scatter is $\approx 0.1$ dex. The total stellar mass exhibits power law scaling with $\alpha_{\text{tot}} \approx 0.6 \pm 0.1$ and scatter of 0.1 dex. The overall efficiency of baryon conversion into stars in individual clusters of a given mass thus shows rather little variation.

4. We show that the total stellar fractions in clusters are only a factor of $\sim 3–5$ lower than the peak stellar fraction reached in $M \approx 10^{12} M_{\odot}$ halos, if the IMF is universal. The difference is only a factor of $\sim 1.5–3$ if the IMF becomes progressively more bottom heavy with increasing mass in early type galaxies, as indicated by several recent observational analyses. This means that the overall efficiency of star formation in massive halos is only moderately suppressed compared to $L_{\star}$ galaxies.

5. We show that stellar mass—halo mass relations derived using abundance matching and reported in recent studies underestimate masses of the BCG galaxies in clusters by a factor of $\sim 2–4$. We argue that this is because these abundance matching analyses used stellar mass functions based on photometry that does not properly account for the outer surface brightness profiles of massive galaxies. We show that $M_{\star}–M$ relation derived using abundance matching with the SMF based on photometry which corrects this problem is in a much better agreement with our derived relation.

6. The new $M_{\star}–M$ relation we derive is significantly steeper than the previously derived relations with significantly larger stellar masses at a fixed halo mass for halos with $M \geq 10^{12} M_{\odot}$. This new relation indicates that suppression of star formation by the AGN feedback and other processes in massive halos is weaker than previously thought. Implementations of these feedback processes in semi-analytic models and simulations thus needs to be re-evaluated.

| Cluster       | $R_{500}$, kpc | $M_{\star}$, $<30$ kpc | $M_{\star}$, $<50$ kpc | $M_{\star}$, $<70$ kpc | $M_{\star}$, $<0.05R_{500}$ | $M_{\star}$, $<0.1R_{500}$ | $M_{\star}$, $<0.25R_{500}$ |
|---------------|----------------|------------------------|------------------------|------------------------|-----------------------------|-----------------------------|-----------------------------|
| A2142         | 1539           | 5.18                   | 7.61                   | 9.61                   | 10.21                       | 14.63                       | 21.69                       |
| A2029         | 1387           | 10.44                  | 15.25                  | 18.84                  | 18.74                       | 25.35                       | 34.09                       |
| A85           | 1235           | 7.12                   | 9.47                   | 10.91                  | 10.38                       | 13.30                       | 21.76                       |
| A1795         | 1196           | 3.85                   | 5.29                   | 6.19                   | 5.76                        | 8.14                        | 12.70                       |
| MKW3s         | 873            | 3.67                   | 4.78                   | 5.56                   | 4.48                        | 6.11                        | 7.80                        |
| A2052         | 840            | 4.35                   | 6.05                   | 7.16                   | 5.45                        | 7.68                        | 10.40                       |
| A1991         | 748            | 4.71                   | 6.75                   | 8.20                   | 5.55                        | 8.48                        | 10.84                       |
| MKW4          | 568            | 4.59                   | 5.99                   | 6.87                   | 4.45                        | 6.33                        | 8.48                        |
| RXJ1159+5531  | 568            | 6.76                   | 8.30                   | 9.12                   | 6.58                        | 8.63                        | 10.38                       |
APPENDIX A

STELLAR MASS–HALO MASS RELATION FROM ABUNDANCE MATCHING

To derive stellar mass–halo mass relation using the abundance matching (AM) ansatz, which was shown to work well in reproducing the observed luminosity dependence of galaxy clustering (Kravtsov et al. 2004; Tasitsiomi et al. 2004; Conroy et al. 2006; Reddick et al. 2013) and other statistics (Vale and Ostriker 2004, 2013a; Behroozi et al. 2010, 2013a; Guo et al. 2010; Moster et al. 2013; Hearin et al. 2013). Specifically, we use the Tinker et al. (2008) calibration of the halo mass function for \( M_{200} \) and \( M_{500} \), which was calibrated using host halos only. To account for subhalos, we correct the host mass function by subhalo fraction, \( f_{sub}(>M) = n_{tot}(>M) - n_{host}(>M) \), to get \( n_{tot}(>M) = \) the mass function that includes both hosts and subhalos. The latter was calculated using current masses for hosts and corresponding masses at the accretion epoch for subhalos using \( z = 0 \) halo catalog halo catalog of Behroozi et al. (2013c) derived from the Bolshoi simulation (Klypin et al. 2011) of \((250h^{-1} \text{Mpc})^3\) volume in the concordance cosmology adopted in this study. The subhalo fraction in the Bolshoi simulation is parametrized as \( f_{sub} = \min(0.35, 0.085(15 - \log_{10} M_{200})) \). The halo mass function derived from the Bolshoi simulation agrees within 5% with the Tinker et al. (2008) parametrization, but the latter is more accurate at the highest halo masses.

We combine two recent calibrations of the SMF by Papastergis et al. (2012) and Baldry et al. (2012) at small masses and Bernardi et al. (2013) at large \( M_* \). We approximate the SMF measured by Papastergis et al. (2012) and Baldry et al. (2012) using double Schechter function given by Eq. (6) of Baldry et al. (2012) with the following parameters: \( \log_{10}(M_*/M_\odot) = 10.66, \phi_1^* = 3.96 \times 10^{-3} \text{Mpc}^{-3}, \alpha_1 = -0.35, \phi_2^* = 6.9 \times 10^{-4} \text{Mpc}^{-3}, \alpha_2 = -1.57. \) These parameters are in general agreement with the best fit parameters derived for the local stellar mass function by Baldry et al. (2012). The SMF of Bernardi et al. (2013) is also parametrized by a double Schechter function (see Eq. (1) of their paper) with parameters for the Sersic fits to galaxy surface brightness profiles (second line in the SMF section of their Table 1): \( \phi_* = 1.04 \times 10^{-2} \text{Mpc}^{-3}, M_* = 9.4 \times 10^7 \text{M}_\odot, \alpha = 1.665, \beta = 0.255, \phi_0 = 6.75 \times 10^{-3} \text{Mpc}^{-3}, M_\gamma = 2.7031 \times 10^7 \text{M}_\odot, \gamma = 0.296. \) It is important to note that the SMF of Bernardi et al. (2013) was estimated using photometry in which particular care was chosen to estimate background for extended massive galaxies. As shown by Bernardi et al. (2013) this results in a significant enhancement of stellar masses for galaxies of \( M_* \gtrsim 10^{11} \text{M}_\odot \). I refer readers to the original papers for further details on how the stellar mass functions were estimated.

We use these two calibrations to construct a combined stellar mass function, \( n(M_*) = \max[n_{B12}, n_{B13}] \), that spans from \( M_* \approx 10^7 \text{M}_\odot \) to \( M_* \approx 10^{12} \text{M}_\odot \). Both stellar mass functions assume the Chabrier IMF and correspond to galaxy surface density at small masses and Bernardi et al. (2013) at \( M_* > 3 \times 10^9 \text{M}_\odot \). Thus, the abundance matching results presented in this paper are determined primarily by this SMF.

We present results both for \( M_* - M \) relation obtained from straightforward abundance matching, \( n(>M) = n(>M) \), without accounting for any scatter between \( M_* \) and \( M \), and relation in which we assume a fixed scatter in \( M_* \) at a fixed \( M \) described by the log-normal pdf, \( p(M_*)|M) = p_{M_*(M)} \):

\[
p_{M_*(M)}dM_* = \frac{\log_{10} e}{\sqrt{2 \pi \sigma_{\log_{10} M_*}}} \times \exp \left[ -\frac{(\log_{10}(M_* - \langle \log_{10} M_* \rangle(M))}{2\sigma^2_{\log_{10} M_*}} \right] dM_*
\]

For the case with scatter the \( M_* - M \) relation obtained using equation

\[
n(M_*) = \int_0^\infty p(M_*|M)n(M)dM,
\]

where we approximate relation between \( \log_{10} M_* \) \( \langle \log_{10} M_* \rangle \) \( M \) and log \( M \) as linear locally \( \log_{10} M_* = a + b\log_{10} M \) and obtain values of \( a_i(M_i), b_i(M_i) \) for a grid of \( M_i \) by minimization of the difference: \( n(M_*) - \int_0^\infty p(M_*|M)n(M)dM \).

Figure 17 shows comparison of the \( M_* - M_{200} \) results obtained as described above with the relations derived by Moster et al. (2013) and Behroozi et al. (2013b) using abundance matching ansatz. Clearly, our relation is much steeper at \( M_{200} \gtrsim 10^{12} \text{M}_\odot \). On cluster mass scale \( M_{200} \gtrsim 10^{14} \text{M}_\odot \), the stellar masses predicted by our relation are a factor of \( \gtrsim 3 \) larger than those predicted by the Moster et al. (2013) and Behroozi et al. (2013b) relations. As we show in Section 3.1 our relation is in much better agreement with direct measurements of the \( M_* - M \) relation at these masses. The main reason for the differences is that we used SMF of Bernardi et al. (2013), which is much shallower at larger \( M_* \) due to increasingly larger stellar masses measured for massive galaxies with their improved photometry analysis method.
Although the differences in the $M_s - M_{200}$ relations shown in Fig. 17 are smaller at smaller masses, they are still substantial even at $M_{200} \approx 10^{12} M_\odot$, as can be seen in the inset showing zoom-in of the region around this mass. For example, for the Milky Way stellar mass of $M_s \approx 5 \times 10^{10} M_\odot$ the corresponding halo mass is $M_{200} \approx 1.3 \times 10^{12} M_\odot$ from our relation, but is $M_{200} \gtrsim 2 \times 10^{12} M_\odot$, but for stellar mass of M31, $M_s \approx 9 \times 10^{10} M_\odot$, corresponds to $M_{200} \approx 3 \times 10^{12} M_\odot$ according to our relation and to $\approx 6 \times 10^{12} M_\odot$ and $\approx 8 \times 10^{12} M_\odot$ according to relations of Moster et al. (2013) and Behroozi et al. (2013b).

For reference, we provide best fit parameters for parametrized form of the $M_s - M$ relation based on the abundance matching with the Bernardi et al. SMF and assuming the WMAP cosmology of the Bolshoi simulation in Table 3. We adopt the five-parameter parametrization of Behroozi et al. (2013b) see their Eq. (3):

$$
\log_{10} M_s = \log_{10} (\epsilon M_1) + f \left[ \log_{10} \left( \frac{M}{M_1} \right) \right] - f(0),
$$

where all masses are in $M_\odot$. We provide fits for relation with and without scatter. For the former, we adopt a constant scatter in $\log_{10} M_s$ at a fixed $M$ of 0.2 dex. The fits approximate the actual relations obtained from abundance matching to $\lesssim 0.05$ dex for halo masses in the range $10^{10} M_\odot < M < 10^{15} M_\odot$. Given the systematic errors in SMF and stellar mass measurements are expected to be $\gtrsim 0.1$ dex, this accuracy should be sufficient for most purposes. For higher accuracy the actual abundance matching calculation should be carried out.

**APPENDIX B**

**ALTERNATIVE BCG STELLAR MASS MEASUREMENTS**

In many recent studies comparing results of simulations with BCG masses stellar content of galaxies attempts are made to model the BCG and its outer regions (the ICL) separately and to mimic the corresponding separation of these components in observational analyses. As we discussed above, it is difficult to separate the inner and outer components of BCGs reliably in practice. At the same time, a number of different definitions is employed in the literature which complicates comparisons of observations and models. We advocate the use of total stellar mass within a given well-defined radii for such comparisons and present stellar masses measured for a range of radii for the BCG galaxies in our nine clusters in Table 4. The typical errors for these masses due to uncertainties of background are $\approx 5-10\%$ for the largest radii and are smaller at smaller radii. Given the small magnitude of these errors we do not quote them in the table. The overall error of stellar masses is dominated by systematic error in conversion of luminosities into stellar mass, which can be as large as $\Delta \log M_s = 0.1-0.2$ dex (e.g., Conroy et al. 2013).

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