Exactly two things to learn from modeling scope ambiguity resolution:
Developmental continuity and numeral semantics

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Abstract

Behavioral data suggest that both children and adults struggle to access the inverse interpretation of scopally-ambiguous utterances in certain contexts. To determine whether the causes of both child and adult difficulty are similar, we extend an existing computational model of children’s scope ambiguity resolution in context. We find that the same utterance-disambiguation mechanism is active in both children and adults, supporting the theory of developmental continuity. Moreover, because adult behavior requires an exact semantics for numerals, we also provide empirical support for this theory of linguistic representation.

Keywords: ambiguity resolution, developmental continuity, language acquisition, numerals, pragmatics, processing, Rational Speech Act model, scope, semantics

1 Introduction

Consider a scenario where two out of three horses jump over a fence. Is the utterance in (1) a reasonable description?

(1) **Every horse didn’t jump over the fence.**

| a. \( \forall \gg \neg \) (surface scope): |
| None of the horses jumped over the fence. |
| b. \( \neg \gg \forall \) (inverse scope): |
| Not all of the horses jumped the fence. |

Adults typically endorse the *every-not* utterance as true, while children typically do not (Musolino, 1998; Lidz and Musolino, 2002; Musolino and Lidz, 2006; Musolino, 2006; Viau et al., 2010). This utterance is scopally ambiguous, involving multiple quantifiers (i.e., *every* and *n’t*). Children’s behavior is non-adult-like at five years old: though the inverse interpretation in (1b) is true, five-year-olds still do not endorse the utterance.

Now, consider a scenario with only two horses, one of which successfully jumps. Is the *two-not* utterance in (2) a reasonable description?

(2) **Two horses didn’t jump.**

| a. \( \exists 2 \gg \neg \) (surface scope): |
| There are two horses that didn’t jump. |
| b. \( \neg \gg \exists 2 \) (inverse scope): |
| It’s not the case that there are two horses that jumped. |

Most adults would not endorse the utterance, despite the inverse interpretation in (2b) being true (Musolino and Lidz, 2003)—that is, it is not the case that two horses jumped (only one did).

This pair of findings underscores that not endorsing a scopally-ambiguous utterance when only the inverse interpretation is true occurs in both children and adults in different contexts. We might therefore wonder about continuity in the development of scope ambiguity resolution: is the cause of child utterance non-endorsement in an *every-not* scenario qualitatively similar to the cause of adult non-endorsement in the *two-not* scenario? If so, this similarity supports developmental continuity: children use the same mechanism as adults when understanding ambiguous utterances in context. The only difference would be that adults are better-equipped to deploy this mechanism, owing perhaps to increased domain-general knowledge and/or cognitive capacities, or to language-specific experience. In contrast, if the underlying causes are different for child and adult utterance non-endorsement, this would suggest developmental discontinuity: children are engaging in a fundamentally different process as they understand ambiguous utterances. So, the development of adult-like behavior would involve ac-
acquiring a new mechanism for resolving ambiguity.

To choose between these accounts, we must understand utterance (non-)endorsement behavior. To that end, Savinelli et al. (2017) articulated a computational model of ambiguity resolution within the Rational Speech Act (RSA) framework (Goodman and Frank, 2016). The model demonstrated the central role of pragmatic factors over processing factors in explaining children’s non-adult-like behavior in every-not contexts like (1). Here, we extend this same model to capture two-not utterance endorsement behavior in adults, identifying the factors that yield the experimentally-observed patterns of behavior.

We begin by reviewing the scope ambiguity resolution findings from Savinelli et al. (2017), together with the experimental results that informed the design of the computational model. Next, we consider the experimental findings from Musolino and Lidz (2003), where adults seem to behave like children in specific contexts. We then extend the model from Savinelli et al. (2017) to capture these new data, and demonstrate support for developmental continuity, with the same utterance-disambiguation mechanism active in both children and adults. Importantly, the complete range of experimentally-observed behavior can only be captured if adults represent two with an exact interpretation, an unexpected finding that informs the debate on numeral semantics.

2 Previous work: Modeling every-not

In the basic truth-value judgment task (TVJT) meant to assess children’s scope disambiguation behavior, children first watch a scene acted out and hear a puppet produce a scopally-ambiguous utterance; then they are asked whether they would endorse the utterance as a true description of the scenario. Children typically do not endorse the ambiguous every-not utterance in the critical context where the surface interpretation is false but the inverse interpretation is true (e.g., a NOT-ALL scenario where two out of three horses jumped over a fence). This behavior has been interpreted as children failing to access the inverse scope interpretation that would make the utterance true.

Interestingly, various alterations to the task setup have yielded more adult-like behavior in children, with higher rates of endorsement for the every-not utterance. These experimental manipulations highlight at least three core factors (two pragmatic, one processing) that underlie children’s behavior in the TVJT: (i) pragmatic: expectations about the experimental world (e.g., how likely successful outcomes are), (ii) pragmatic: expectations about the Question Under Discussion (QUD; e.g., were all outcomes successful?), and (iii) processing: the accessibility of the inverse scope (i.e., the ease by which the logical form is either derived or accessed in real time).

To capture and independently manipulate the contributions of each of these factors, Savinelli et al. (2017) modeled ambiguity resolution for every-not utterances within the Bayesian RSA framework (Goodman and Frank, 2016). They found that when it comes to understanding non-adult-like behavior in the TVJT, there is likely a stronger role for the pragmatics of context management (as realized in prior beliefs about world state and QUD) than for grammatical processing (as realized in the prior on scope interpretations), although there may be a role for both. So, children’s failure to endorse scopally-ambiguous every-not utterances in NOT-ALL contexts likely stems from their beliefs about the experimental world (e.g., whether actors are a priori likely to succeed) and about the topic of conversation (e.g., whether the conversational goal is to determine if all the actors succeeded), rather than an inability to grammatically derive or access the inverse scope interpretation in real time.

Perhaps most interesting was the prediction that the highest rates of utterance endorsement (i.e., adult-like behavior) occur when resolving the scope ambiguity is irrelevant for communicating successfully about the NOT-ALL world. This occurs when expectations about the world state favor total success, or when the QUD asks if all of the actors succeeded. In either case, both scope interpretations serve to inform a listener, either that the a priori likely total-success world state does not hold or that the answer to the all? QUD is no.

The explanation for utterance non-endorsement (i.e., non-adult-like behavior) is similar: Savinelli et al. (2017)’s model predicts the lowest rates of utterance endorsement in NOT-ALL scenarios when neither interpretation is useful for successful communication, either because the interpretation is false (surface) or because beliefs about the pragmatic context render the interpretation un-informative (inverse). Thus, the TVJT utterance non-endorsement data previously used to demon-
strate children’s difficulty with inverse scope calculation in fact require no disambiguation at all if the goal is informative communication. Instead, children simply need the ability to manage the pragmatic context so they can recognize the potential informativity of these ambiguous utterances. Notably, considerations of pragmatic context have long played a role in the design and interpretation of the TVJT (e.g., Crain et al., 1996). Savinelli et al. (2017) take the extra step of formally articulating specific pragmatic factors and the role they play in children’s apparent difficulty with ambiguous utterances in the TVJT.

3 Experimental two-not results

Musolino and Lidz (2003) (ML2003) demonstrated that adults are sensitive to some of the same experimentally-manipulated factors as children when it comes to endorsing scopally-ambiguous utterances. Like us, ML2003 were interested in developmental continuity: are child and adult ambiguity resolution behavior in context qualitatively similar? To investigate this, they conducted three TVJTs.

The goal of the first TVJT was to determine which interpretation adults preferred when they endorsed a scopally-ambiguous utterance in context. For example, adults heard “Cookie Monster didn’t eat two pizza slices” in a context where both interpretations were true, such as Cookie Monster eating one of three available pizza slices (surface: it’s not the case he ate two = true; inverse: there are two he didn’t eat = true). Importantly, they were then asked to explain why they endorsed the utterance so that their preferred scope interpretation could be inferred. For example, if their answer referred to Cookie Monster eating only one slice, then it was assumed that they accessed the surface interpretation (surface: he only ate one, so it’s not the case he ate two). However, if their answer referred to the two slices Cookie Monster did not eat, then it was assumed that they accessed the inverse interpretation (inverse: there are two he didn’t eat). All participants endorsed the utterance, and their explanations indicated a strong surface scope bias (75% surface, 7.5% inverse, 17.5% unclear from explanation). ML2003 interpreted this finding as evidence that adults prefer the surface scope interpretation when both interpretations are true in context. It could then be that children’s non-endorsement behavior, if due to a preference for the surface scope interpretation, is driven by a stronger version of this same preference.

In the second TVJT, adults heard an utterance like (2) (e.g., Two frogs didn’t jump over the rock) in two different contexts. The first context included two actors (e.g., frogs), with one actor successfully completing the action (e.g., frog1 jumping over the rock while frog2 does not). In this 1-of-2 context, the surface interpretation is false (only frog2 did not jump, so it is false that two frogs didn’t jump), but the inverse interpretation is true (only frog1 did jump, so it is indeed not the case that two frogs jumped). Yet, adults had low endorsement (endorsement rate: 27.5%).

In the second context, there were four actors. For example, four frogs attempted to jump over a rock; two jumped (frog1, frog2) and two did not (frog3, frog4). In this 2-of-4 context, the surface interpretation of the scopally-ambiguous utterance is true because frog3 and frog4 did not jump. However, the inverse interpretation is false because frog1 and frog2 did indeed jump. Here, adults had an endorsement rate of 100%.

ML2003 interpreted this asymmetry of endorsement between the two contexts as a strong surface scope preference in adults. According to this explanation, non-endorsement occurs in the 1-of-2 context because only the inverse scope is true; in contrast, endorsement occurs in the 2-of-4 context because only the surface scope is true. That is, both these patterns would result because adults favor the surface interpretation. While we find this account compelling, we note that there are other differences between the two contexts that might lead to the observed asymmetry. For example, it could be that the seemingly benign change from two to four total actors affects the pragmatic context. Another variable is the potential ambiguity present in the numeral semantics, which only occurs in the 2-of-4 context. In either case, exploring the effects of these factors in a formal model of TVJT behavior can clarify the process underlying utterance disambiguation.

Returning to the question of continuity, while the observable behavior appears qualitatively the same in children and adults (i.e., a non-endorsement preference when only the inverse scope is true), it remains unclear whether the underlying cause of this behavior is the same. To

\[1\text{A topic discussed in more detail in the following section.}\]
evaluate this, ML2003 conducted a third TVJT with adults in 1-of-2 contexts, involving an experimental manipulation from Lidz and Musolino (2002) that children are known to be sensitive to. This manipulation is implemented as an explicit linguistic contrast clause before the scopally-ambiguous utterance, such as the bolded material in (3).

(3) **Two frogs jumped over the fence but**

two frogs didn’t jump over the rock.

Adults responded the same way as the children from Lidz and Musolino (2002), shifting to strong endorsement in the 1-of-2 context (endorsement rate: 92.5%; cf. 27.5% endorsement without the explicit contrast). Yet, as ML2003 note themselves, it is not obvious why the adult endorsement rate increases when the linguistic contrast is present. According to ML2003, the linguistic contrast creates the positive expectation necessary to make the negation in the later clause felicitous (Wason, 1965; Musolino and Lidz, 2003). However, it remains unclear how exactly the context creates the positive expectation. There are multiple ways this information could impact the context. For example, the positive expectation could arise because of a change either in the pragmatic factor of world knowledge or in the pragmatic factor of the QUD. Specifically, the affirmative statement could alter the listener’s beliefs about how successful frogs are known to be in the experimental world. This affirmative statement also potentially changes the listener’s expectations about the QUD: because both frogs were successful before, the topic of conversation might now be focused on whether both frogs were successful again. Both these effects could generate a context that makes the negated clause more informative.

Without knowing the factors responsible for endorsement behavior, it is difficult to determine whether the same factors are operating in both children and adults, and whether the underlying representation of two matters. Computational modeling can help determine why these two behavioral patterns occur: (i) adult sensitivity to the pragmatic contrast manipulation, and (ii) asymmetry in endorsement behavior between 1-of-2 and 2-of-4 contexts in the absence of that pragmatic contrast. In the next section, we extend Savinelli et al. (2017)’s model of utterance disambiguation to handle these empirical data.

### 4 Modeling two-not

Savinelli et al. (2017)’s model of ambiguity resolution is conceived within the Bayesian Rational Speech Act (RSA) framework (Goodman and Frank, 2016), which views language understanding as a social reasoning process. A pragmatic listener \( L_1 \) interprets an utterance by reasoning about a cooperative speaker \( S_1 \) who is trying to inform a literal listener \( L_0 \) about the world. The model is a “lifted-variable” extension in which the ambiguous utterance’s literal semantics gets parameterized by interpretation-fixing variables (e.g., the relative scope of the quantificational elements; Bergen et al., 2012; Lassiter and Goodman, 2013; Scontras and Goodman, 2017). Hearing an ambiguous utterance, the pragmatic listener \( L_1 \) reasons jointly about the true state of the world (e.g., how many frogs successfully jumped), the scope interpretation speaker \( S_1 \) had in mind (i.e., surface, inverse), as well as the likely QUD that the utterance addresses (e.g., did all frogs succeed?). To generate testable predictions, participant TVJT behavior is modeled as a pragmatic speaker \( S_2 \)’s (relative) endorsement of an utterance about an observed situation (cf. Degen and Goodman, 2014; Tessler and Goodman, 2016).

That is, this model predicts whether a speaker \( S_2 \) would endorse the scopally-ambiguous utterance as a description of the observed state. \( S_2 \) decides this by reasoning about whether a pragmatic listener \( L_1 \) (who is reasoning about a speaker \( S_1 \) reasoning about a literal listener \( L_0 \)) would arrive at the correct world state after hearing the utterance.

We take world states \( w \in W \) to consist of a collection of \( n \) individuals (e.g., frogs), each of which either succeeds or fails at the relevant task (e.g., jumping over a rock). The world success baseline \( b_{suc} \) determines the probability that an individual will succeed. We assume a simple truth-functional semantics where an utterance \( u \) denotes a mapping from world states to truth values (\( \text{Bool} = \{ \text{true}, \text{false} \} \)). We parameterize this truth function so that it depends on the scope interpretation \( i \in I = \{ \text{inverse}, \text{surface} \} \): \( W \rightarrow \text{Bool} \). We consider two alternative utterances \( u \in U \): the null utterance (i.e., saying nothing at all, and so choosing not to endorse the utterance) and the scopally-ambiguous utterance \( amb \) (e.g., “Two frogs didn’t jump over the rock”).

To fix the utterance semantics, we must consider potential ambiguity introduced by the nu-
meral in cases where the number of relevant individuals $n$ exceeds the numeral’s value. For example, consider the positive utterance “Two frogs jumped over the rock.” If we assign an exact (=) semantics to two, the sentence will be true only when two frogs succeeded. If we assign an at least (≥) semantics, the sentence will be true when two or more frogs succeeded. In worlds with only two frogs, the = vs. ≥ distinction makes no difference: the sentence will be true in the world where both frogs succeed, and false in all other worlds. However, in a world with four frogs, the numeral semantics will define different truth-functional mappings. With the = semantics, the sentence is true in any world where two frogs—but not more—succeed. With the ≥ semantics, the sentence is true in a larger set of worlds, where two or more frogs succeed.

To evaluate the potential contribution of utterance semantics to the 1-of-2 vs. 2-of-4 asymmetry, we consider two different sets of utterance alternatives, one with ambul null and another with ambul true. So, $U_{null} = \{null, ambul null\}$ and $U_{true} = \{null, ambul true\}$. The utterance semantics in (4) shows that scope parameterization $i$ only impacts the truth conditions for ambul utterances.2

(4) Utterance semantics $[u]^i$:

- a. $[null]^i = true$
- b. $[ambul_{null}]^i = true$ if $i = inverse_{null}$
- c. $[ambul_{true}]^i = true$ if $i = inverse_{true}$

where:

- $[inverse_{null}] = \lambda w. \neg \exists x: \{x = 2 \land x \subseteq success(w)\}$
- $[surface_{null}] = \lambda w. \exists x: \{x = 2 \land x \subseteq success(w)\}$
- $[inverse_{true}] = \lambda w. \neg \exists x: \{x = 2 \land x \subseteq success(w)\}$
- $[surface_{true}] = \lambda w. \exists x: \{x = 2 \land x \subseteq success(w)\}$

We consider five potential QUDs $q \in Q$, three from the original Savinelli et al. (2017) model: (i) “What happened with the frogs?” (what-happened?), (ii) “Did all the frogs succeed?” (all?), and (iii) “Did none of the frogs succeed?” (none?). We also consider two additional QUDs specific to the two-not utterance: (iv) “Did exactly two frogs succeed?” (two?), and (v) “Did at least two frogs succeed?” (two≥?).

The QUDs serve as projections from the inferred world state to the relevant dimension of meaning, so that $q: W \rightarrow X$ (Kao et al., 2014a,b). In practice, the QUDs establish partitions on the possible world states, as shown in (5). For example, the all? QUD partitions the world space in two: the unique world in which all frogs succeeded (true) and all other possible worlds (false).

(5) QUD semantics $[q]$:

- a. $[what\text{-}happened?] = \lambda w. w$
- b. $[all?] = \lambda w. success(w) = w$
- c. $[none?] = \lambda w. success(w) = \emptyset$
- d. $[two\text{-}null?] = \lambda w. |success(w)| = 2$
- e. $[two\text{-}true?] = \lambda w. |success(w)| \geq 2$

Literal listener $L_0$ has prior uncertainty about the true state, $P(w)$. $L_0$ updates beliefs about $w$ conditioned on the the literal semantics, and restricts prior beliefs to those worlds that $[u]^i$ maps to true. The function $\delta_{[u]^i}(w)$ maps the Boolean truth value to a probability, 1 or 0.

$$P_{L_0}(w|u,i) \propto \delta_{[u]^i}(w) \cdot P(w)$$

To capture the notion that communication proceeds relative to a specific QUD $q$, $L_0$ must infer not only the true world state $w$, but also the value of the QUD applied to that world state, $[q](w) = x$.

$$P_{L_0}(x|u,i,q) \propto \sum_w \delta_{x=[q](w)} \cdot P_{L_0}(w|u,i)$$

Speaker $S_1$ chooses an utterance $u$ in proportion to its utility in communicating about the true world state $w$ with respect to the QUD $q$, $[q](w) = x$. Thus, the speaker maximizes the probability that $L_0$ arrives at the intended $x$ from $u$. This selection is implemented via a softmax function (exp) and free parameter $\alpha$, which controls how rational the speaker is in utterance selection.

$$P_{S_1}(u|w,i,q) \propto \exp(\alpha \cdot \log(L_0(x|u,i,q)))$$

Utterance interpretation happens at the level of the pragmatic listener $L_1$, who interprets an utterance $u$ to jointly infer the world state $w$, the interpretation $i$, and the QUD $q$. We model ambiguity resolution as pragmatic inference over an underspecified utterance semantics (i.e., the interpretation variable $i$). To do this, $L_1$ inverts $S_1$’s model, and so the joint probability of $w$, $i$, and $q$ is proportional to the likelihood of $S_1$ producing utterance $u$ given world state $w$, interpretation $i$, and QUD $q$, as well as the priors on $w$, $i$, and $q$.

$$P_{L_1}(w,i,q|u) \propto P_{S_1}(u|w,i,q) \cdot P(w) \cdot P(i) \cdot P(q)$$
To model the utterance endorsement implicit in TVJT, we need an additional level of inference. Pragmatic speaker $S_2$ observes the true world state $w$ and selects $u$ by inverting the $L_1$ model, thus maximizing the probability that a pragmatic listener would arrive at $w$ from $u$ by summing over possible interpretations $i$ and QUDs $q$ for world $w$.

$$P_{S_2}(u|w) \propto \exp(\log \sum_{i,q} P_{L_1}(w, i, q|u))$$

To generate model predictions for adult sensitivity to the pragmatic contrast manipulation and the 1-OF-2 vs. 2-OF-4 asymmetry, we fix various model parameters. For 1-OF-2 data, we set the number of individuals $n$ to 2; for 2-OF-4 data, we set $n$ to 4. The $S_1$ speaker rationality parameter $\alpha > 0$ is set to 2.5 (i.e., the same value in the every-not simulations in Savinelli et al., 2017). The priors $P(w)$ and $P(q)$ correspond to expectations for the discourse context (i.e., likely world states or QUDs). In the default case, we set these priors to be uniform over their possible values, with the individual success baserate $b_{suc}$ set to 0.5 and the relevant QUDs having equal probability. The interpretation prior $P(i)$ corresponds to how easy it is to access the inverse scope interpretation. In the default case, $P(\text{inverse}) = P(\text{surface}) = 0.5$. Importantly, to better understand utterance endorsement behavior with scopally-ambiguous utterances, we can independently manipulate the values of the priors on $W$, $Q$, and $I$, and observe their impact on utterance endorsement.

5 Results

Recall the empirical phenomena we are trying to capture: (i) the dramatic increase in endorsement rates in the 1-OF-2 context when an explicit contrast is present, and (ii) the stark asymmetry in utterance endorsement rates between 1-OF-2 and 2-OF-4 contexts in the absence of that explicit contrast. We report results for each in turn.

5.1 The explicit contrast effect for 1-OF-2

Following Savinelli et al. (2017), we attempt to capture the increase in ambiguous utterance endorsement rates by systematically manipulating the pragmatic and processing factors, as implemented in the relevant priors.

For the world state prior (Figure 1, left), we manipulate baserate $b_{suc}$, which determines an actor’s chance of success. Holding the QUD and scope priors at their default values, we see a marked increase in endorsement of the ambiguous utterance in the 1-OF-2 context as prior beliefs about frog success increase. Utterance endorsement is at its lowest (33%) when prior knowledge suggests that frogs are particularly unlikely to succeed; endorsement is at its highest (86%) when frogs are very likely to succeed.

For the QUD prior (Figure 1, center), we selectively favor specific QUDs by assigning a 0.9 probability to the favored QUD and dividing the remaining probability equally among the others. Since the two? QUDs are equivalent to the all? QUD in the 1-OF-2 context, we omitted the two? QUDs in the 1-OF-2 context. Holding the other priors at their default values, endorsement rates increase from favoring the none? QUD (35%) to favoring the what-happened? QUD (46%) to favoring the all? QUD (64%).

For the scope prior (Figure 1, right), we manipulate the prior probability of the inverse interpretation while holding the other factors at their default values. We see an increase in utterance endorsement as the probability of inverse increases, from a low of 40% to a high of 57%.

Each manipulation qualitatively captures the response pattern from ML2003, and replicates the results of Savinelli et al. for every-not. However, as observed by Savinelli et al., the pragmatic factors controlling world and QUD beliefs have a much more pronounced effect than the processing factor controlling scope access; the model’s world prior baserate manipulation comes closest to capturing the experimentally-observed effect of explicit contrast manipulation (i.e., 27.5% base endorsement vs. 92.5% endorsement with the explicit contrast). We can amplify the effect of the world baserate manipulation by allowing it to interact with the other factors.

As discussed in Section 3, the early success explicit contrast manipulation possibly affects two aspects of the disambiguation calculus: it could increase expectations for success and shift the topic of conversation to whether total success was achieved again. Figure 2 plots the interaction of the world and QUD priors, together with the effect of scope. The low-endorsement baseline (27.5%) most likely results from low expectations for success ($b_{suc} = 0.1$) and QUD uncertainty (QUD: uniform), together with a moderate to low probability of accessing the inverse scope ($P(\text{inv}) = 0.1$ or 0.5). From this baseline, we implement...
the effect of the explicit contrast manipulation by increasing success expectations \(b_{\text{suc}} = 0.9\) and shifting the topic of conversation to whether total success occurred (QUD: all?). This manipulation results in a dramatic increase in utterance endorsement, irrespective of scope.

To summarize, if the explicit contrast clause impacts a listener’s beliefs about the frogs’ chance of success (increasing \(b_{\text{suc}}\)) or the QUD (favoring all?), then the model predicts the endorsement rate should increase. Notably, both of these manipulations make the two-not scopally-ambiguous utterance more informative for a listener. In the case of the world state manipulation, two-not—from either scope interpretation— informs the listener that her prior beliefs about total frog success do not hold. Similarly with the QUD manipulation favoring all?, both scope interpretations answer this question in the negative (i.e., it is not the case that all (two) frogs succeeded).

5.2 The 1-OF-2 vs. 2-OF-4 asymmetry

If the factors identified for capturing the experimentally-observed effect of the explicit contrast are indeed active in utterance disambiguation (i.e., to validate their explanatory power), we would expect the very same factors and values to additionally capture the ceiling-level endorsement rate in the 2-OF-4 context without the explicit contrast.

Recall the baseline 1-OF-2 values from Figure 2: low expectations for success \(b_{\text{suc}} = 0.1\) and QUD uncertainty (QUD: uniform). To model the 2-OF-4 context, we change the number of actors \(n\) to 4 and additionally manipulate whether the exact (=) or at-least (≥) semantics applies, as they diverge when there are more than two actors in the context (see section 4). This decision impacts both the utterance semantics and the relevant set of QUDs (e.g., if ≥ semantics gets used, then the two? QUD is included in the set of potential QUDs). As shown in Figure 3, we do indeed predict high endorsement with the same parameter value baseline, but only with exact utterance semantics and a low probability of accessing the inverse scope \(P(\text{inv}) = 0.1\). In this case, we find an endorsement rate of 92%.

6 Discussion

Our model of ambiguity resolution in context captures the effect of the explicit contrast manipulation observed in adults in ML2003, and notably...
also captured the same effect in children (Savinelli et al., 2017). This parallelism—sensitivity to the pragmatic context in both children and adults across different contexts—suggests that the same disambiguation mechanism is active in both children and adults. Adults seem better able to charitably interpret less supportive pragmatic contexts (i.e., the original every-not scenarios); yet, there remain scenarios (i.e., certain two-not contexts) where even adult abilities are exceeded. We interpret the common underlying mechanism as support for developmental continuity in scope ambiguity resolution, with no qualitative shift required.

In addition to supporting the developmental continuity hypothesis, this model also suggests why manipulations like the explicit contrast clause work. The pragmatic variables capture the explicit contrast manipulation because they create a situation where the ambiguous two-not utterance is still informative despite the ambiguity. When the utterance provides the listener with information that diverges from her prior beliefs, the ambiguous two-not utterance becomes more informative, more useful, and therefore more endorsable.

The model also seamlessly captures ML2003’s results from the 2-of-4 context: with the very same parameter values that yield low endorsement rates for 1-of-2 contexts, the model predicts the high endorsement observed for 2-of-4 contexts. The only change is increasing the number of relevant individuals from two to four. This exploration of the 1-of-2 vs. 2-of-4 contexts allows us to refine our understanding of the potential sources of child and adult behavior. Savinelli et al. (2017)’s findings suggested that pragmatic factors alone are capable of capturing the non-adult-like behavior in children and the extension in the current model captures the explicit contrast effect in adults; however, the processing factor of scope (in particular, disfavoring the inverse scope) is needed to account for ML2003’s 2-of-4 results. This finding supports ML2003’s conclusion, namely that adults have a strong preference for surface interpretations of two-not utterances. Combined with the appropriate pragmatic context, that preference has the potential to drive the endorsement asymmetry between the 1-of-2 and 2-of-4 contexts. Whether this surface interpretation preference in two-not contexts is also something children share remains an open empirical question; experimental results for every-not do not answer this question definitively (Viau et al., 2010; Savinelli et al., 2017).

Importantly, the present model requires one more ingredient to account for the 1-of-2 vs. 2-of-4 difference in adult behavior: an exact numeral semantics (in contrast to an at-least semantics; cf. Geurts, 2006; Breheny, 2008; Spector, 2013; Kennedy, 2015). While the underlying utterance semantics is not something easy to manipulate in an experiment, it is exactly the kind of variable we can systematically explore in a computational model. By doing so here, we are able to show the necessity of an exact semantics in generating observable adult behavior. This provides empirical support, coming from computational modeling, for theories about the semantics of numerals. In particular, the only way to account for the observed adult behavior is if adults interpret two utterances as meaning exactly two.

To sum up, these findings underscore the complexity of information involved in interpreting scopally-ambiguous utterances, including the literal semantics of the utterances involved, processing factors that affect interpretation accessibility, pragmatic factors that affect the potential informativity of the utterance, and the recursive social reasoning between speakers and listeners. Here, we find evidence for the impact of both pragmatic and processing factors, and in particular how a specific confluence of values for these factors yields the observed adult utterance endorsement behavior in multiple contexts. The fact that pragmatic factors can have such a pronounced effect on their own accords with previous computational findings about the cause of children’s utterance endorsement behavior in context, thereby highlighting the developmental continuity in pragmatic reasoning from childhood to adulthood. Moreover, the fact that the processing factor of scope access is crucial for explaining adult behavior in certain contexts motivates experimental work with children to see if their behavior is likewise affected by this processing factor in similar contexts. The fact that only the exact utterance semantics is capable of yielding the observed behavior provides empirical support in favor of this theory of representation for numerals. More broadly, we have demonstrated how computational modeling can help us refine our theories about different aspects of language, including theories of language understanding, language development, and language representation.
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