Time-reversal symmetry violation in molecules induced by nuclear magnetic quadrupole moments

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Recent measurements in paramagnetic molecules improved the limit on the electron electric dipole moment (EDM) by an order of magnitude. Time-reversal (T) and parity (P) symmetry violation in molecules may also come from their nuclei. We point out that nuclear T,P-odd effects are amplified in paramagnetic molecules containing deformed nuclei, where the primary effects arise from the T,P-odd nuclear magnetic quadrupole moment (MQM). We perform calculations of T,P-odd effects in the molecules TaN, ThO, ThF\textsuperscript{+}, HfF\textsuperscript{+}, YbF, HgF, and BaF induced by MQMs. We compare our results with those for the diamagnetic TlF molecule, where the T,P-odd effects are produced by the nuclear Schiff moment. We argue that measurements in molecules with MQMs may provide improved limits on the strength of T,P-odd nuclear forces, on the proton, neutron and quark EDMs, on quark chromo-EDMs, and on the QCD \(\theta\)-term and CP-violating quark interactions.

In order to explain the matter-antimatter asymmetry in the universe, additional sources of CP-violation (or equivalently T-violation, assuming CPT symmetry) are required, beyond those in the Standard Model of particle physics \[1\]. Measurements of T,P-violating electric dipole moments (EDMs) are an efficient way to search for this type of new physics \[2\]. For example, the parameter space for CP-violation in supersymmetric theories is very strongly limited by EDM measurements \[3,4\].

Measurements of nuclear T,P-odd effects have focused on heavy diamagnetic atoms \[5–8\] and molecules \[9\]. In these systems, the EDM of the nucleus is entirely screened by electrons (the Schiff theorem \[10\]) and contributes negligibly to the measurable EDM. Instead, here the observable EDM is generated by the nuclear Schiff moment (SM). The SM is an intra-nuclear charge distribution, generated by T,P-violating interactions within the nucleus, which can induce an atomic/molecular EDM by polarizing the bound electrons \[11,12\]. The SM has size \(\sim r_N^2d_N\) where \(r_N\) (\(d_N\)) is the nuclear radius (EDM). Since \(r_N\) is very small compared to the electron orbital size, the atomic EDM produced by the nuclear SM is much smaller than \(d_N\). By contrast, the magnetic interaction between nuclear moments and electrons is not screened. The lowest T,P-odd magnetic moment is the magnetic quadrupole moment (MQM). It was shown in \[11\] that in paramagnetic atoms and molecules, the nuclear MQM produces a larger EDM than does the SM (see also \[13,14\]), for the same underlying sources of CP-violation. Moreover, the MQM has a collective nature and is significantly enhanced in deformed nuclei (like the ordinary electric quadrupole moment) \[15\].

Unfortunately, it has been difficult to devise experiments sensitive to MQMs, and hence to take advantage of these mechanisms for enhanced effects of T,P-odd hadronic physics. There are several problems \[2\]. Use of paramagnetic rather than diamagnetic systems generally leads to much shorter spin coherence times and hence drastically reduced energy resolution. Susceptibility to magnetic noise is also greatly increased in paramagnetic systems.

Recently, however, there have been experimental advances that could be used to exploit the intrinsic advantages of MQMs. In particular, it has become possible to perform EDM measurements using molecules in paramagnetic \(3\Delta_1\) electronic states. Due to a cancellation of electronic orbital and spin magnetic moments their net magnetic moment is on the order of a nuclear magneton \[16\]. They also have \(\Omega\)-doublet substructure, which both allows full polarization in modest external electric fields and provides a means to cancel many systematic errors \[17,18\]. Intense, slow molecular beams \[19,20\] and techniques for spin-precession measurements both on such beams \[21\] and on trapped molecular ions \[22\] have been developed. Using these methods, recently the limit on the electron EDM (eEDM) was improved by an order of magnitude using the \(3\Delta_1\) state of \(^{232}\)ThO \[23\]; substantial further improvements in sensitivity are anticipated \[22,23\].

In this paper, we point out the possibility to use this type of molecular state to search for T,P-odd interactions in the hadronic sector. This approach takes advantage of the dramatically enhanced energy shifts associated with the strong electric polarization of molecules, as was exploited in older experiments searching for the SM of \(^{205}\)Tl in TIF \[2\]. However, it also uses the enhanced effects of the MQM, especially in deformed nuclei, to further boost the sensitivity relative to experiments using atomic \(^{199}\)Hg, where measurements of the SM now place the strongest limits on most underlying effects \[2\].

The MQM also appears more amenable to a reliable interpretation than the SM, due to the differences in nu-
clear structure that give rise to these effects. In the expression for the SM there are two terms that have close values and opposite sign [11]. This makes the result sensitive to corrections such as those due to finite nuclear size [24] and many-body effects [23, 27]. Also, in EDM experiments using nuclei with a valence neutron (e.g. $^{199}$Hg), the direct valence nucleon contribution is zero and the SM is generated primarily by polarization of the nuclear core by its T,P-odd interaction with the valence neutron [25]. This makes calculations of the SM especially sensitive to many-body corrections, which significantly suppress the final results and make them unstable [23, 24].

For the MQM a valence nucleon gives the main contribution, so the result should be less sensitive to many-body corrections (the T,P-odd core polarization contribution to the MQM was estimated in [28]).

The eEDM, SM, and MQM contributions to the T,P-odd effects in paramagnetic diatomic molecules are described by the effective molecular Hamiltonian [11]:

$$H = W_d d_e S \cdot n + W_Q Q T I \cdot n - \frac{W_M M}{2(I+1)} S \Omega n. \quad (1)$$

Here $n$ is a unit vector along the molecular axis, $I$ is the nuclear spin, $S$ is the effective electronic spin, $d_e$ is the eEDM, $Q$ is the nuclear SM, and $M$ is the nuclear MQM, with components

$$M_{i,k} = 3M/[2I(I-1)] T_{i,k}, \quad (2)$$

where $T_{i,k} = I_I I_k + I_k I_I - \frac{2}{3} \delta_{i,k} I(I+1)$. For the maximal nuclear spin projection $I_z = I$ along $n$, we have $M_{zz} = M$ and the MQM energy shift in Eq. (1) is $-\frac{1}{2}W_M M S_z$. This shift is quadrupled by switching the directions of the external fields [29]. The value of $S$ is defined as $S = |\Omega|$, where $\Omega = J_e \cdot n$ is the projection of the total electronic angular momentum $J_e$ on the molecular axis. The parameters $W_d$, $W_Q$ and $W_M$ must be found from molecular electronic structure calculations; some useful equations for them are presented in [11].

**Nuclear calculations of MQM.** The MQM of a nucleus can arise both due to the EDMs of the constituent nucleons, and due to intra-nuclear T,P-odd forces. The calculation of the MQM produced by a valence nucleon EDM was done in Ref. [30]. The MQM produced by T,P-odd nuclear forces was calculated in [11] (see also [31]). It is important that T,P-odd nuclear forces produce T,P-odd nuclear moments 1-2 orders of magnitude larger than those caused by nucleon EDMs [11]. Following [11, 30] we can present the MQM of a valence nucleon as

$$M = M_0^d (2I-1) t_I, \quad (3)$$

$$M_0^d = [d_e + \xi_v (\mu_v - q_v)] h/(m_pc), \quad (4)$$

where $t_I = 1$ for $I = l + \frac{3}{2}$ and $t_I = -\frac{1}{j(I+1)}$ for $I = l - \frac{1}{2}$, $I$ and $l$ are the total and orbital angular momenta of the valence nucleon denoted by $v = p, n$; $d_e$ is the valence nucleon EDM, $\xi_v = -2 \cdot 10^{-21} \eta_v (e \cdot cm)$, $\eta_v$ is the dimensionless strength constant of the T,P-odd nuclear potential $H_{T,P} = \eta_v G_F/(23/2m_p)(\sigma \cdot \nabla \rho)$, $\rho$ is the total nucleon number density, $G_F$ is the Fermi constant, $m_p$ is the proton mass, and the nucleon magnetic moments and charges are $\mu_p = 2.79, q_p = 1$ and $\mu_n = -1.91, q_n = 0$.

The T,P-odd nuclear forces are dominated by $\eta_0$ meson exchange. Therefore, we may express the strength constants via the strong $\pi NN$ coupling constant $g = 13.6$ and three T,P-odd $\pi NN$ coupling constants $\tilde{g}_T$ corresponding to the isospin channels $T = 0, 1, 2$: $\eta_0 = -\eta_\pi \approx 5 \cdot 10^6 g(\tilde{g}_1 + 0.4\tilde{g}_2 - 0.2\tilde{g}_0)$. The numerical coefficient comes from $[G_F m_\pi^2/(21/2)^{-1}] = 6.7 \cdot 10^6$ times the factor 0.7 corresponding to the zero range reduction of the finite range interaction due to the $\pi_0$-exchange [11, 32]. As a result, we obtain

$$M_0^d(g) = [g(\tilde{g}_1 + 0.4\tilde{g}_2 - 0.2\tilde{g}_0)] + d_e/(1.4 \cdot 10^{-14} e \cdot cm)] \cdot 3 \cdot 10^{-28} e \cdot cm^2. \quad (5)$$

In the numerical coefficient here we included two additional correction factors. First, more accurate numerical calculations in a Saxon-Woods potential [11, 32] give larger values of MQM (by a factor $\sim 1.2$) than the simple analytical solution in Eq. (1). Second, many-body corrections reduce the effective strength constants $\eta_v$ of the T,P-odd potential by $\sim 1.5$ times [15, 33].

Finally, we can use previously derived relations between underlying sources of CP-violation and the nuclear T,P-odd forces, to express the MQM in terms of these more fundamental quantities. For example, the QCD CP violation parameter $\theta$ induces a nuclear T,P-odd force described by the relation $g \tilde{g}_0 = -0.37 \theta$ [34], leading to a valence nucleon MQM:

$$M_0^d(\theta) \approx M_0^d(0) \approx 2 \cdot 10^{-29} \theta e \cdot cm^2. \quad (6)$$

Contributions of $\tilde{g}$ to the MQM via the EDMs of the neutron $(d_n = 1.2 \cdot 10^{-16} \tilde{g} e \cdot cm)$ and proton $(d_p \approx -d_n)$ are an order of magnitude smaller. Note that the valence contributions of $\tilde{g}_0$ and $\tilde{g}_\pi$ to the MQM are suppressed by the small factor $(N - Z)/A \approx 0.2$, where $N$ and $Z$ are the neutron and proton numbers and $A = N + Z$. The contribution of the T,P-odd core polarization [25] has no such suppression and may increase the value of MQM in terms of $\tilde{g}_0$ and $\tilde{g}_\pi$.

Similarly, we can express MQM in terms of the $u$ and $d$ quark EDMs $d_{u,d}$ and chromo-EDMs $\tilde{d}_{u,d}$ using the relations $g \tilde{g}_1 = 4 \cdot 10^{15}(\tilde{d}_u - \tilde{d}_d)/cm, g \tilde{g}_0 = 0.8 \cdot 10^{15}(\tilde{d}_u + \tilde{d}_d)/cm, d_p = 1.1 e(\tilde{d}_d + 0.5d_d) + 1.4d_d + 0.35d_d, d_u = 1.1 e(\tilde{d}_d + 0.5\tilde{d}_u) + 1.4d_d + 0.35d_d$. We find finally

$$M_0^d(\tilde{d}) \approx M_0^d(\tilde{d}) \approx 1.2 \cdot 10^{-28}(\tilde{d}_u - \tilde{d}_d) \cdot e \cdot cm. \quad (7)$$

Note that the contributions of $d_u$ and $d_p$ to this expression are only a few percent and are neglected.
TABLE I: Nuclear MQMs $M$ derived from Eqs. (23–35) and the orbital occupation numbers given in [33]. The values of $M_{0}^{2}$ and $M_{0}^{3}$ in terms of different constants of CP-violating interactions and EDM are given in Eqs. (4–7). The values for the spherical nuclei $^{139}$Ba and $^{201}$Hg have been presented for comparison; note the typical factor of 10–20 enhancement for the deformed nuclei.

| Nucleus | $M$ | Nucleus | $M$ |
|---------|-----|---------|-----|
| $^{173}$Ta | $-14M_{0}^{2} - 11M_{0}^{3}$ | $^{177}$Th | $0M_{0}^{2} - 19M_{0}^{3}$ |
| $^{179}$Hf | $-10M_{0}^{2} - 10M_{0}^{3}$ | $^{179}$Hf | $-19M_{0}^{2} - 14M_{0}^{3}$ |
| $^{201}$Hg | $0M_{0}^{2} + 2M_{0}^{3}$ | $^{137}$Ba | $0M_{0}^{2} - 1.2M_{0}^{3}$ |

For spherical nuclei, the quantum numbers needed to find the valence nucleon contribution to the nuclear MQM are related to the nuclear spin $I$ and parity $P$. For example, the nucleus $^{201}$Hg has $I^{P} = 3^{-}$, with one valence neutron in a $p_{3/2}$ state, $I = I + \frac{1}{2}$, $l_{z} = 1$, and $M = 2M_{0}^{2}$.

The situation is more complicated in deformed nuclei, where the MQM has a collective nature. Here, about $A^{2/3}$ nucleons belong to open shells due to the shell splitting by the strong quadrupole field. The MQM of a deformed nucleus is in the “frozen” frame (rotating together with the nucleus), $M_{z}^{\text{nucl}}$, is given by [15]:

$$M_{z}^{\text{nucl}} = \sum_{I, I_{z}} M_{z z}^{\text{single}}(I, I_{z}, l) n(I, I_{z}, l),$$

(8)

where $M_{z z}^{\text{single}}(I, I_{z}, l)$ is given by Eqs. (3) and (2) and $n(I, I_{z}, l)$ are the single-nucleon orbital occupation numbers, which may be found in Ref. [36]. The MQM in the laboratory frame $M \equiv M_{z}^{\text{lab}}$ can be expressed via the MQM in the rotating frame:

$$M_{z}^{\text{lab}} = \frac{I_{z}(2I_{z} - 1)}{(I_{z} + 1)(2I_{z} + 3)} M_{z}^{\text{nucl}},$$

(9)

where $I_{z}$ is the total nuclear spin. Values for the MQMs of various nuclei are given in Table I.

Calculations of the MQM effects in molecules. The first estimates of the effects of MQM in many heavy molecules were performed in Ref. [11]. Calculations of the constant $W_{M}$ in Eqs. (11) for BaF, YbF, and HgF were done in Refs. [37, 38] using a semiempirical approach based on measured molecular hyperfine structure constants.

The parameters $W_{d}$ and $W_{M}$ depend on the molecular wave function in the vicinity of the heavy nucleus, where it can be expanded in partial waves. Up to normalization factors, at short distances these partial waves resemble valence atomic orbitals of the heavy atom. The dominant matrix element for $W_{d}$ is between $s_{1/2}$ and $p_{1/2}$ waves. The electronic operator for the MQM interaction has higher tensor rank and the dominant matrix element for $W_{M}$ is between $s_{1/2}$ and $p_{3/2}$ waves. For the $s_{1/2}$ orbital at large distances from the nucleus the waves $p_{1/2}$ and $p_{3/2}$ must combine into a non-relativistic $p_{z}$ wave, which has the form: $|p_{z}, \omega\rangle = -\frac{2\omega}{\sqrt{3}}|p_{1/2}, \omega\rangle + \sqrt{\frac{2}{3}}|p_{3/2}, \omega\rangle$, where $\omega = \pm \frac{1}{2}$ is projection of the total angular momentum $j_{z}$ along $n$ (for a many-electron molecular state, $\sum_{i} \omega_{i} = \Omega$). This equation links the amplitudes of the relativistic partial waves $p_{1/2}$ and $p_{3/2}$. Because of this, the amplitudes in the dominant matrix elements for $W_{d}$ and $W_{M}$ are also linked. Consequently, to first approximation the ratio of $W_{M}$ and $W_{d}$ depends on the nuclear charge $Z$ only:

$$W_{M} = \frac{9R_{M}(Z)}{20r_{0}}aZR_{Q}(Z)W_{d},$$

(10)

where $R_{M}(Z)$ and $R_{d}(Z)$ are the relativistic factors for MQM and eEDM presented in [11, 39] and $r_{0}$ is Bohr radius. This expression holds to 20% accuracy for the molecules BaF, YbF, and HgF, where $W_{d}$ and $W_{M}$ were calculated in [27, 38].

Metastable $^{3}\Delta_{1}$ state of the molecules ThO, TaN and ions HfF$^{+}$, ThF$^{+}$. The EDM parameter $W_{d}$ was calculated for the molecule ThO [40, 41] and for the ions HfF$^{+}$ [42, 44] and ThF$^{+}$ [41, 45]. We use these results and relation (10) to estimate parameter $W_{M}$ for these systems (see Table III). On the Dirac-Fock level relation (10) holds nicely for atomic ions Hf$^{+}$ and Th$^{+}$ and we expect these estimates of $W_{M}$ to be accurate to about 30%.

There are no calculations of $W_{d}$ for TaN. The electronic state $^{3}\Delta_{1}$ was studied theoretically and experimentally in Ref. [46] and was found to include two uncoupled electrons in $\sigma$ and $\delta$ orbitals. This makes it similar to the $^{3}\Delta_{1}$ state of the molecule ThO. However, here calculations indicate that the $\sigma$ orbital is primarily a mixture of the $6s$ and $5d$ orbitals of the heavy atom (Ta), with no admixture of the $p$ wave reported in [46]. The closest analogue to TaN is YbF. Because of the larger $Z$ and larger binding energies, the atomic MQM matrix element for Ta is 1.6 times bigger than for Yb. On the other hand, the large admixture of the $d$ wave rather than the $p$ wave should lead to smaller molecular matrix elements. Thus, as a very rough estimate for TaN we take the value of $W_{M}$ from Ref. [38] for YbF and divide it by 2 to account for the difference in $\Omega$.

In Table III we summarize our results for molecules that are used, or considered for EDM experiments. One of the best limits on the eEDM comes from measurements on YbF molecule in $^{3}\Sigma_{1/2}$ state [29]. Hence we include calculations of MQM shifts in three such species, which were calculated in [38]. We express the shifts in terms of the fundamental underlying CP-violating physical quantities $d_{p}$, $\tilde{\theta}$, and $d_{u,d}$. The current limits on these quantities are given in Ref. [3]: $|d_{p}| < 8.6 \cdot 10^{-22} \text{ e- cm}$, $|\tilde{\theta}| < 2.4 \cdot 10^{-10}$, and $|d_{u} - d_{d}| < 6 \cdot 10^{-27} \text{ cm}$. The values of the frequency shifts produced by the nuclear MQMs are sufficiently large to compete in the improvement of limits on the proton EDM $d_{p}$, on the $\theta$-term, and on the difference
of the quark chromo-EDMs ($\tilde{d}_u - \tilde{d}_d$). To quantify this statement, we note that the current accuracy in measurements of the energy shift produced by the eEDM in ThO is 700 μHz [23]; it is anticipated that this may be ultimately improved by as much as ~2 orders of magnitude [47]. Similar sensitivity is anticipated in measurements based on trapped molecular ions in $^3\Delta_1$ states including HFF$^+$ or ThF$^+$ [22]. For comparison, for the molecule $^{181}$TaN the limits on the proton EDM, $|\tilde{\theta}|$, and $|\tilde{d}_u - \tilde{d}_d|$ correspond to shifts $|W_{M,M}| < 260 \mu$Hz, 120 μHz, and 180 μHz, respectively.

**Comparison with TIF molecule.** It is useful to compare the sensitivity to underlying sources of CP-violation for these molecular systems with MQM contributions, to that in the dianionic molecule TIF. The observable T,P-odd effect in TIF is mainly produced by the nuclear SM Q. The SM potential for a finite nucleus has been found in Ref. [24] (unfortunately, in all molecular calculations $^{18}F$ [52] the authors used the finite nucleus Coulomb potential, but the Schiff moment potential remained point-like, $U = -4\pi\varepsilon_0 \frac{Q^2}{r} (I \cdot \nabla \delta(r))$ [11, 12]). In a simple valence nucleon model the nuclear potential is equal to [11, 49] $Q^2 = \frac{d_v + d_q}{10} \left( t_1 + \frac{1}{T+1} \right) r^2 \frac{5}{8} t_1 r_Q^2$, where $r_v^2$ and $r_q^2$ are the mean squared valence nucleon and total charge distribution radii. For $^{205}$TI and $^{203}$TI nuclei the valence proton is in $3s_{1/2}$ state, i.e. $I = \frac{1}{2}$ and $t_1 = 1$, and $Q^2 = -(d_v + \xi_v g_v) \frac{R}{T}$, where $R \equiv r_v^2 - r_q^2$. A more accurate numerical SM calculation including the T,P-odd core polarization gives $Q^2 = -(d_v + \xi_v g_v) \frac{R}{T} + (8.4 \eta_{pn} - 7.2 \eta_{pp}) \cdot 10^{-21} \, \text{e} \cdot \text{cm} \cdot \text{fm}^2 / 6$, where $\eta_{pn}$ and $\eta_{pp}$ are proton-neutron and proton-proton interaction constants, $\eta_{pp} = \frac{4}{3} \eta_{pp} + \frac{8}{3} \eta_{pn}$ [25]. Different numerical nuclear calculations give $-6 \, \text{fm}^2 < R < 5 \, \text{fm}^2$ [2, 49]. In Ref. [49] the authors selected the largest of 4 results of B.A. Brown nuclear calculations $R = 2.9 \, \text{fm}^2$, and this value was used in all recent molecular calculations $[50, 52]$ where the proton dipole moment $d_p$ was extracted from the TIF experiment [4].

The nuclear EDM actually gives a small but non-zero contribution to the T,P-odd frequency shift if one takes a magnetic interaction into account [11, 48]. The valence formula for the nuclear EDM was derived in [11]: $d_N = (d_u - c\xi(q - \frac{2}{3})) t_1$. Using the molecular matrix elements calculated in ref. [52] we obtain the SM (volume) contribution $d^V = W_{QQ}$ and the magnetic effect contribution $d^M$ to the T,P-odd frequency shift in TIF:

$$d^V = -3.4 \cdot 10^{-3} \, \text{Hz} \left[ \frac{R}{\text{fm}^2} + \frac{8 \eta_{pn} - 7 \eta_{pp}}{9} \right],$$

$$d^M = 2.0 \cdot 10^{-3} \, \text{Hz} \left[ \frac{10^2 d_p}{\text{e} \cdot \text{cm}} + 0.7 \eta_{pp} + 0.5 \eta_{pp} \right].$$

Using $\eta_{pp} \approx 5 \cdot 10^6 g(\bar{g}_1 - 2\bar{g}_2 + \bar{g}_0)$, $\eta_{pp} \approx 5 \cdot 10^6 g(\bar{g}_1 + 2\bar{g}_2 - \bar{g}_0)$, we obtain the frequency shift $\nu$ for $^{205}$TI in terms of different T,P-odd constants:

$$\nu(\bar{g}) = -1.0 \cdot 10^5 \, \text{Hz} \, g(-0.08\bar{g}_1 - 5.32\bar{g}_2 + 2.6\bar{g}_0);$$

$$\nu(\bar{g}) = 1.0 \cdot 10^5 \, \text{Hz} \, \bar{g} / \eta_{pp} = 2 \cdot 10^2 \, \text{Hz} \, (\frac{d_u + d_d}{\text{cm}}).$$

Note that the sensitivity to $\bar{g}_0$ and $\bar{g}$ is probably overestimated here since it comes from the T,P-odd core polarization, which in the case of the atomic Hg SM is strongly suppressed by the many-body corrections $[27, 28]$. These TIF results may also be used as an estimate of the SM contribution in the molecules which we considered in this paper, taking into account the scaling $Z^2 A^{2/3} R_Q$, where $R_Q$ is the relativistic factor for the Schiff moment $[11]$. The SM contribution is 1-2 orders of magnitude smaller than the MQM contribution. The experiment with TIF [48] gave the T,P-odd frequency shift $\nu = d^V + d^M = -0.13 \pm 0.22 \, \text{mHz}$. This gives limits $|\bar{g}| < 4 \cdot 10^{-9}$ and $|d_u + d_d| < 2 \cdot 10^{-24} \, \text{cm}$.

**Conclusion.** We find that the sensitivity to nuclear T,P-odd effects is high in paramagnetic molecules containing deformed nuclei. If measurements of EDM-like frequency shifts can be made with sensitivity an order of magnitude better than in the recent eEDM experiment using ThO molecules, then limits on several underlying parameters of hadronic T,P-violation can be improved. The molecule $^{181}$TaN, not considered before for EDM measurements, looks especially promising. Methods similar to those used in the ThO experiment should be applicable; even better sensitivity may be possible since the lifetime of the metastable $^3\Delta_1$ state should be much longer in TaN than in ThO (due to its lower excitation energy $[40, 53]$). However, further work on the molecular and nuclear structure of TaN will be needed to verify the estimates given here.

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