Research Article

Heat and Mass Transfer in Reduction Zone of Sponge Iron Reactor

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Abstract
Numerical prediction is performed on reduction zone of iron ore reactor which is a part of counter current gas-solid reactor for producing sponge iron. The aim of the present study is to investigate the effect of reduction gas composition and temperature on quality and capacity of sponge iron products through mathematical modeling arrangement and simulation. Simultaneous mass and energy balances along the reactor lead to a set of ordinary differential equation which includes kinetic equations. Kinetic equations of reduction of hematite to iron metal, methane reforming, and water gas shift reaction are taken into account in the model. Hydrogen and carbon monoxide are used as reduction gas. The equations were solved by finite element method. Prediction shows an increase in H2 composition while an attenuation of CO produces higher metallization degree. Metallization degree is also increased with an increase in gas inlet temperature. It is found that reduction gas temperature over 973°C (1246 K) is not recommended because the formation of sticky iron will be initiated.

1. Introduction

Sponge iron product quality in direct Reduced iron (DRI) plant can be increased by rising reduction gas temperature and composition of reactant in reduction gas. The rising of temperature will accelerate reaction flow rate which in turn can raise reaction conversion as shown by Zhang and Ostrovski [1]. However, the temperature rising can also bring disadvantage due to the formation of total carbon on the product. The increasing of reactant composition which is consisted of H2 and CO in reduction gas will also increase product quality as reported by many researchers (e.g., [2–4]). The optimum composition of reduction gas must be determined to obtain the highest quality.

The investigation of temperature and composition of reduction gas is carried out by analyzing the performance of sponge iron reactor which in turn can predict the profitable optimum condition of reactor. However, since the reactor analysis is difficult to be executed directly in the field plant, it will need a simulator as support instrument. This simulator can be designed by arrangement of heat and mass transfer equation inside the reactor to reproduce reactor data from the field. By solving heat and mass transfer equations, the effect of reduction gas on the performance of reactor is studied.

Some iron ore reactor models are proposed in a few literatures. Iron ore reactor model proposed by Aguilar et al. [5] is referred for fixed bed reactor. The model is derived based on unsteady state condition. Parisi and Laborde [6] proposed a model for moving bed counter current reactor. The model is limited on reduction zone of iron ore reactor, and only reduction reactions are considered in the model, in which plug flow is used as an approach for the model.

Another related model is formulated on direct reduction shaft furnace for producing sponge iron from iron ore as proposed by Takenaka et al. [7]. In their model, reduction rate equations are derived from the three-interface model which involves both mass and heat balances. Srinivasan [8] develops a model for reduction iron oxides by carbon. This model in which only the global direct reduction reactions are taken into account and methane reforming and water gas shift reaction are ignored, is formulated on a circulating fluidized bed reactor.

The kinetics of direct reduction reaction plays an important role in sponge iron reduction zone mathematical model. Unreacted core model proposed by Levenspiel [9] is widely used for kinetics model of iron reduction in which the reaction occurs first at the outer skin of the particle. The zone of reaction then moves into the solid and may leave behind
shown as follows: Pellet. In general, hydrogen and carbon monoxide are used as reducer and the corresponding reduction reactions are occurring between reduction gas and iron ore. These reactions which are called reduction reactions are shown in Figure 1. In the reduction zone, there are some zones, which are referred to as reduction, isobaric, and cooling zones. The simple scheme of iron ore reactor is arranged on the gas and solid phases. Heat and mass transfer equations are formulated to perform the temperature changes, and (v) the plug flow is used to approach a model for gas and solid phases. By considering the above assumptions, heat and mass balance equations can be stated as follows:

2. Reactor Modeling

Iron ore reactor is a moving bed reactor to produce sponge iron product from iron ore. Gas and solid phases are passed in counter current. In general, sponge ore reactor is divided by 3 zones, which are referred to as reduction, isobaric, and cooling zones. The simple scheme of iron ore reactor is shown in Figure 1. In the reduction zone, there are some reactions occurring between reduction gas and iron ore pellets. These reactions which are called reduction reaction will extract iron metal from the ore to create sponge iron product. These reactions occur on the surface of iron ore pellet. In general, hydrogen and carbon monoxide are used as reducer and the corresponding reduction reactions are shown as follows:

\[3 \text{Fe}_2\text{O}_3 + \text{CO(H}_2) \leftrightarrow 2 \text{Fe}_3\text{O}_4 + \text{CO}_2(\text{H}_2\text{O}) \] (1)

\[\text{Fe}_3\text{O}_4 + \text{CO(H}_2) \leftrightarrow 3 \text{FeO} + \text{CO}_2(\text{H}_2\text{O}) \] (2)

\[\text{FeO} + \text{CO(H}_2) \leftrightarrow \text{Fe} + \text{CO}_2(\text{H}_2\text{O}) \] (3)

Methane reforming and water gas shift reactions also occur in the gas phase based on the composition of reduction gas and temperature through reaction as follows:

\[\text{CH}_4 + \text{H}_2\text{O} \leftrightarrow \text{CO}_2 + \text{H}_2 \] (4)

\[\text{CO}_2 + \text{H}_2 \leftrightarrow \text{CO} + \text{H}_2\text{O} \] (5)

Mathematical model of reduction zone in iron ore reactor is arranged on the gas and solid phases. Heat and mass transfer equations are formulated to perform the temperature and concentration of gas and solid phases, respectively. The modeling is also carried out by employing kinetics model. Note that iron reduction, methane reforming, and water gas shift reactions are taken into account in the model.

The mass and energy equations are formulated by assuming (i) steady-state operating conditions, (ii) no heat loss over the wall of reactor reduction zone, (iii) the iron ore pellet consumption is governed by the unreacted shrinking core model, (iv) the enthalpy is calculated based on temperature changes, and (v) the plug flow is used to approach a model for gas and solid phases. By considering the above assumptions, heat and mass balance equations can be stated as follows:

\[\dot{n}_{\text{gas}} \frac{dC_{\text{H}_2}}{dz} = r_{\text{methanation}}(\text{CH}_4, \text{H}_2, T_{\text{gas}}), \] (6)

\[\dot{n}_{\text{gas}} \frac{dC_{\text{H}_2}}{dz} = r_{\text{WGSR}}(\text{CO}, T_{\text{gas}}) + r_{\text{methanation}}(\text{CH}_4, \text{H}_2, T_{\text{gas}}) (7)\]

\[r_{\text{WGSR}}(\text{CO}, T_{\text{gas}}) = -n_s \cdot \text{FeO-reduction(H}_2, T_{\text{solid}}), \] (7)

\[\frac{dC_{\text{CO}}}{dz} = r_{\text{WGSR}}(\text{CO}, T_{\text{gas}}) \] (8)

\[\dot{n}_{\text{gas}} \frac{dC_{\text{Fe}}}{dz} = n_s \cdot \text{FeO-reduction(CO, H}_2, T_{\text{solid}}), \] (9)

\[\dot{n}_{\text{solid}} \frac{dC_{\text{Fe}_3\text{O}_4}}{dz} = n_s \cdot \text{FeO-reduction(CO, H}_2, T_{\text{solid}}), \] (10)

\[\dot{n}_{\text{solid}} \frac{dC_{\text{FeO}}}{dz} = n_s \cdot \text{FeO-reduction(CO, H}_2, T_{\text{solid}}), \] (11)

\[\dot{n}_{\text{solid}} \frac{dC_{\text{Fe}}}{dz} = n_s \cdot \text{FeO-reduction(CO, H}_2, T_{\text{solid}}), \] (12)

\[\frac{dT_{\text{gas}}}{dz} = \frac{A_{\text{sp}} \cdot h \cdot (T_{\text{solid}} - T_{\text{gas}})}{M_{\text{gas}} \cdot C_{p_{\text{gas}}}} + \frac{R_{\text{gas}} \cdot \sum [H_i r_j]}{M_{\text{gas}} \cdot C_{p_{\text{gas}}}}, \] (13)

\[\frac{dT_{\text{solid}}}{dz} = \frac{A_{\text{sp}} \cdot h \cdot (T_{\text{solid}} - T_{\text{gas}})}{M_{\text{solid}} \cdot C_{p_{\text{solid}}}} - \frac{\sum [H_i r_j]}{M_{\text{solid}} \cdot C_{p_{\text{solid}}}}. \] (14)

Equations (6)–(8) are mass balance equations for gas phase, while (9)–(12) are for solid phase. Heat balance equations for gas and solid phase are expressed by (13) and (14), respectively. Notation \(A_{\text{sp}}\) is pellets surface area per unit reactor volume, \(h\) is convection heat transfer coefficient, and \(M\) is molar flow rate.

Heat capacities \(C_p\) of gas and solid phases in (13) and (14) are calculated based on the temperature changes in each phase. On the gas phase, heat capacity value is calculated based on the mixing of heat capacity of CO and \(H_2\). The other components such as \(H_2O\), \(CH_4\), \(CO_2\), and \(N_2\) are omitted because they have small fraction compared to CO and \(H_2\).

The heat capacity of gas phase is evaluated as follows:

\[C_{p_{\text{gas}}} = \left( \frac{C_{p_{\text{CO}}}}{C_{\text{CO}} + C_{\text{H}_2}} \right) C_{p_{\text{CO}}} + \left( \frac{C_{p_{\text{H}_2}}}{C_{\text{CO}} + C_{\text{H}_2}} \right) C_{p_{\text{H}_2}}. \] (15)
The values of standard reaction enthalpy at 298 K \((H_{R(298)})\) for each reaction are obtained from Chemical Sciences [12]. Reaction heat capacity \((Cp_R)\) is also calculated for each reaction by using

\[
Cp_R = \sum_i b_iCp_{i\text{-reactant}} - \sum_j b_jCp_{j\text{-product}},
\]

where \(i\) and \(j\) refer to reactant and product number, respectively. Notation \(b\) is stoichiometric coefficient for each reactant and product.

Heat transfer coefficient, \(h\), is determined by using the correlation proposed by Furnas [14]. He investigates heat transfer value from a stream of air to a bed of iron pellets covered with a thin coating of iron oxides. The temperature experiments are set up to 1023 K. The equation proposed by Furnas [14] is as follows:

\[
h = 6.91 \times 10^{-3} \times G_f^{0.75} \times T \times G^{-1.56} \times 5.67826.
\]

Notation \(r\) in (6)–(14) is referred to as kinetic expression of every reaction which occurs in reduction zone. There are three kinetic equations involved in the model, namely, a kinetic equation of methanation reaction, a kinetic equation of water gas shift reaction, and a kinetic equation of reduction reaction. Kinetic expression of methanation reaction \((r_{\text{methanation}})\) is adopted from Munster and Grabke [15] given by

\[
r_{\text{methanation}} = f_{\text{methanation}} k_d a_0 \exp \left( \frac{-E_A^m}{RT} \right) \left( \frac{P_{CH_4}}{P_{H_2}} \right).
\]

Here, the values of activation energy \((E_A)\) and preexponential constant \((k_d)\) are the same as those adopted in the literature [15]. Constant, \(a_0\), is expressed as \(p_{H_2O}/p_{H_2}\). Note that correction factor \(f_{\text{methanation}}\) proposed here is added so as to correct the value of preexponential constant.

Many researchers propose kinetic equations for water gas shift reaction. The validity of kinetic model is to get results which have a good agreement with reference data. Some kinetics models are valid for low-temperature reaction while some others are not. Bustamante et al. [16] carried out on the temperature range of 1148–1198 K whose condition is similar to that of the present study. Their kinetic model is shown as follows:

\[
r_{\text{WGSR}} = f_{\text{WGSR}} k_a \exp \left( \frac{-E_A^s}{RT} \right) \left( \frac{p_{H_2O}}{p_{H_2}} \right)^{0.33} \left( C_{CO_2} \right).
\]

Here, the value of \(k_a\) is corrected by correction factor \(f\).

Kinetic equations of reduction reaction in iron ore are created based on shrinking core model for spherical particles. The formulations of kinetics equation are derived based on the model proposed by Levenspiel [9]. Although many literatures propose the models such as Mondal et al. [10], Iguchi and Yokomoto [11], and Shi et al. [17]; among them, Levenspiel formulates the model in more detail by considering every step which is close with reality. Figure 2 shows the visualization of shrinking core model for iron reduction. Basically, 5 steps take place during reaction, as explained in Levenspiel [9].
(a) Diffusion of gaseous reactants (CO and H₂) through
the film surrounding the particle to the surface of the
solid.

(b) Diffusion of CO and H₂ through the blanket of ash to
the surface of the unreacted core of iron pellet.

(c) Reaction of CO and H₂ with iron ore at reaction
surface through
\[
3\text{Fe}_2\text{O}_3 + \text{CO(H}_2) \rightarrow 2\text{Fe}_3\text{O}_4 + \text{CO}_2(\text{H}_2\text{O}) \quad (24)
\]
\[
\text{Fe}_3\text{O}_4 + \text{CO(H}_2) \rightarrow 3\text{FeO} + \text{CO}_2(\text{H}_2\text{O}) \quad (25)
\]
\[
\text{FeO} + \text{CO(H}_2) \rightarrow \text{Fe} + \text{CO}_2(\text{H}_2\text{O}) \quad (26)
\]

(d) Diffusion of gaseous products (CO₂ and H₂O)
through the ash back to gas film.

(e) Diffusion of gaseous products through the gas film
back into the main body of fluid.

The kinetic equation of each step must be combined
to get overall kinetic expression for each component involved
in reduction reaction. Therefore, the expression of kinetic
equation of each step must be defined in the same manner.

Since the rate of mass transfer (gas diffusion) on steps (a),
(b), (d), and (e) can be defined as the flow of material unit
surface, or
\[
Q_{\text{diffusion}} = -\frac{1}{S} \frac{dN_{\text{gas}}}{dt}, \quad (27)
\]

the reaction step (step (c)) must similarly be defined as
\[
Q_{\text{reaction}} = -\frac{1}{S} \frac{dN_i}{dt}. \quad (28)
\]

Based on those steps, we can formulate the overall kinetic
equation based on 3 main equations; those are as follows.

1) Diffusion through Gas Film Control (Steps (a) and (c)). If
gas CO or H₂ diffuses through a stagnant film onto surface of
ash as shown in Figure 3, the flux of material can be defined
as the flow of gas unit surface, or
\[
Q_{\text{gas}} = -\frac{1}{S} \frac{dN_{\text{gas}}}{dt} = D \frac{\Delta C}{\Delta r} = \frac{D}{\Delta r} (C_{\text{CO or H}_2} - C_{\text{ash}})
\]
\[
= k_{\text{film}} (C_{\text{CO or H}_2} - C_{\text{ash}}), \quad (29)
\]

where \( S \) is surface area (m²), \( N \) is mole amount of CO
or H₂ in mole (\( k_{\text{film}} \)) is gas film kinetic constant (m/sec),
C is concentration (mole/m³), and \( D \) is molecular diffusion
coefficient (m²/sec). The same equation can also be applied
for diffusion of gas product (CO₂ and H₂O).

On the ash surface, the flux diffusion can also be stated as
\[
Q_{\text{ash}} = -\frac{1}{S} \frac{dN_{\text{CO or H}_2}}{dt} = k_{\text{ash}}C_{\text{ash}}, \quad (30)
\]

where \( k_{\text{ash}} \) is kinetic constant on ash. Since \( C_{\text{ash}} \) is difficult
to be measured, this variable must be disappeared in (29) or
(30). At steady state, the flow rate to the surface is equal to
the reaction rate at the surface, thus
\[
Q_{\text{gas}} = Q_{\text{ash}}, \quad (31)
\]
\[
k_{\text{film}} (C_{\text{CO or H}_2} - C_{\text{ash}}) = k_{\text{ash}}C_{\text{ash}}.
\]
Therefore,
\[ C_{\text{ash}} = \frac{k_{\text{film}}}{k_{\text{film}} + k_{\text{ash}}} C_{\text{CO or H}_2}. \]  (32)

If we insert (32) to (29) or (30), we will get
\[ Q_{\text{gas}} = -\frac{1}{S} \frac{dN_{\text{CO or H}_2}}{dt} = k_{\text{ash}} \frac{k_{\text{film}}}{k_{\text{film}} + k_{\text{ash}}} C_{\text{CO or H}_2} \]
\[ = k_{\text{GAS}} C_{\text{CO or H}_2}, \]  (33)

where \( k_{\text{GAS}} \) is overall kinetic constant on gas film. Equation (33) then will be used as kinetic expression of diffusion through gas film control.

(2) Diffusion through Ash Layer Control (Steps (b) and (d)). If the flux of gas within the ash layer is expressed by Fick’s law for equimolar counter diffusion, then we will have
\[ Q = \frac{1}{S} \frac{dN_{\text{CO or H}_2}}{dt} = \varphi_e \frac{dC_{\text{CO or H}_2}}{dr}, \]  (34)

where \( \varphi_e \) is effective diffusion coefficient of gaseous reactant in the ash layer.

If we define \( S = 4\pi r^2 \), we will get
\[ -\frac{dN_{\text{CO or H}_2}}{dt} = 4\pi r^2 \cdot \varphi_e \frac{dC_{\text{CO or H}_2}}{dr}, \]
\[ -\frac{dN_{\text{CO or H}_2}}{dt} \int_{R_p}^{R_c} \frac{dr}{r^2} = 4\pi \cdot \varphi_e \int_{C_{\text{CO or H}_2} \text{ at } R_p}^{0} dC_{\text{CO or H}_2}. \]  (35)

Then, by integrating (34), we get
\[ -\frac{dN_{\text{CO or H}_2}}{dt} \left( \frac{1}{R_c} - \frac{1}{R_p} \right) = 4\pi \varphi_e C_{\text{CO or H}_2}. \]  (36)

If we multiply both sides with \( 1/A_p \) where \( A_p \) is pellet surface area and define \( A_p = 4\pi R_p^2 \) where \( R_p \) is pellet radius, we get
\[ -\frac{1}{A_p} \frac{dN_{\text{CO or H}_2}}{dt} \left( \frac{1}{R_c} - \frac{1}{R_p} \right) \]
\[ = \frac{1}{4\pi R_p^2} 4\pi \varphi_e C_{\text{CO or H}_2} \]
\[ = \frac{1}{R_p^2} \left( \frac{1}{R_c} - \frac{1}{R_p} \right) \times \varphi_e C_{\text{CO or H}_2}. \]  (37)

Equation (38) then will be used as kinetic expression of diffusion through ash layer control.

(3) Chemical Reaction Controls (Step (c)). There are 6 main components which involve in reduction reaction; those are hematite (\( \text{Fe}_2\text{O}_3 \)), magnetite (\( \text{Fe}_3\text{O}_4 \)), wustite (\( \text{FeO} \)), metal iron (Fe), carbon monoxide (CO), and hydrogen (H\(_2\)). The reactions are assumed pseudo-first order; that is, the rate of reaction for each component is formulated as follows.

(a) \( \text{Fe}_2\text{O}_3 \):
\[ -\frac{1}{A_p} \frac{dN_{\text{Fe}_2\text{O}_3}}{dt} = \frac{1}{4\pi R_p^2} \frac{dN_{\text{Fe}_2\text{O}_3}}{dt} = k_1 C_{\text{Fe}_2\text{O}_3}, \]  (39)

where \( R_p \) is unreacted core radius in pellet.

If we multiply each side by \( 1/A_p \) and define \( A_p = 4\pi R_p^2 \), we get
\[ -\frac{1}{A_p} \frac{dN_{\text{Fe}_2\text{O}_3}}{dt} = \frac{R_p^2}{R_p^2} k_1 C_{\text{Fe}_2\text{O}_3}. \]  (40)

(b) \( \text{Fe}_3\text{O}_4 \):
\[ -\frac{1}{A_p} \frac{dN_{\text{Fe}_3\text{O}_4}}{dt} = \frac{R_p^2}{R_p^2} (-X \cdot k_1 C_{\text{Fe}_2\text{O}_3} + k_2 C_{\text{Fe}_3\text{O}_4}). \]  (41)

(c) \( \text{FeO} \):
\[ -\frac{1}{A_p} \frac{dN_{\text{FeO}}}{dt} = \frac{R_p^2}{R_p^2} (-Yk_2 C_{\text{Fe}_3\text{O}_4} + k_3 C_{\text{FeO}}). \]  (42)

(d) Fe:
\[ -\frac{1}{A_p} \frac{dN_{\text{Fe}}}{dt} = \frac{R_p^2}{R_p^2} (-Zk_3 C_{\text{FeO}}). \]  (43)

(e) CO:
\[ -\frac{b}{A_p} \frac{dN_{\text{CO}}}{dt} = \frac{R_p^2}{R_p^2} V_1 (k_1 C_{\text{Fe}_2\text{O}_3} + k_2 C_{\text{Fe}_3\text{O}_4} + k_3 C_{\text{FeO}}). \]  (44)

(f) H\(_2\):  
\[ -\frac{b}{A_p} \frac{dN_{\text{H}_2}}{dt} = \frac{R_p^2}{R_p^2} V_2 (k_1 C_{\text{Fe}_2\text{O}_3} + k_2 C_{\text{Fe}_3\text{O}_4} + k_3 C_{\text{FeO}}). \]  (45)

Notations \( X, Y, \) and \( Z \) shown in (41), (42), and (43), respectively, represent the weight coefficient, while \( V_1 \) and \( V_2 \) on (44) and (45) represent equilibrium conditions.

Kinetic reaction constants \( k_1, k_2, \) and \( k_3 \), respectively, refer to reaction as
\[ 3\text{Fe}_2\text{O}_3 + CO(H_2O) \xrightarrow{k_1} 2\text{Fe}_3\text{O}_4 + CO_2(H_2O) \]  (46)
\[ \text{Fe}_3\text{O}_4 + CO(H_2O) \xrightarrow{k_2} 3\text{FeO} + CO_2(H_2O) \]  (47)
\[ \text{FeO} + CO(H_2O) \xrightarrow{k_3} \text{Fe} + CO_2(H_2O). \]  (48)

If we combined the 3 main equations shown above, we get the individual equation for each component involved in reduction reaction as written below.

(a) \( \text{Fe}_2\text{O}_3 \):
\[ -\frac{1}{A_p} \frac{dN_{\text{Fe}_2\text{O}_3}}{dt} = b k_{\text{GAS}} C_{\text{CO or H}_2} + \frac{b \varphi_e C_{\text{CO or H}_2}}{R_p^2 \left( \frac{1}{R_c} - \frac{1}{R_p} \right)} \]
\[ + b \frac{R_p^2}{R_p^2} (k_1 C_{\text{CO or H}_2} C_{\text{Fe}_2\text{O}_3}). \]  (49)
isobaric zone is \(4700 \text{ m}^3/\text{hour}\). If their temperature and concentration are multiplied by the number of pellets per unit volume \(n_p\) to get the overall reaction rate.

Reaction constants \(k_1, k_2, k_3\) in (50)–(55) are modeled based on Arrhenius method which is stated as

\[
k_i = k_o \cdot \exp \left[\frac{-E_A}{RT}\right].
\]

Here, as for two variables unknown in (56), those are pre-exponential constant \(k_o\) and activation energy \(E_A\). Note that the corresponding values are different for each reduction reaction by CO and \(H_2\). Many literatures focus on the comparison of \(E_A\) values rather than \(k_o\), because the variation of \(k_o\) values is large and highly dependent on research condition. The value of activation energy \(E_A\) is important to get good result. The \(k_o\) and \(E_A\) values used in this research are adopted from Aguilar et al. [5]. The formulations of each \(k\) are shown in Table 1.

Overall kinetic constant on gas film \(k_{GAS}\) is calculated based on formulation proposed by Parisi and Laborde [6] as stated as

\[
k_{GAS} = 0.00225 \exp \left[\frac{-14700}{82.06T}\right].
\]

while effective diffusion coefficient \(\varphi_e\) is calculated using

\[
\varphi_e = \frac{e_p \cdot D}{\tau_p}.
\]

Considering the unreacted core model, it is possible to relate the radius of the unreacted core \(r_c\) with the solid conversion \(\alpha\) by

\[
R_c = \left(\frac{R^3 - \alpha \cdot M_w}{n_p 4 \pi \rho}\right)^{1/3},
\]

where

\[
\alpha = \left(\frac{C^0_{CO} - C_{CO}}{C^0_{H_2} - C_{H_2}}\right).
\]

Simulation is carried out on sponge iron production capacity of 2500 tone/day. Reduction gas flow rate required is about 125000 m\(^3\)/hour, while leaking cooling gas flow rate from isobaric zone is 4700 m\(^3\)/hour.

Calculation of the model is executed by using finite element method. The calculation is divided by many segments along height of reduction zone. Figure 4 shows the simulation algorithm to solve mathematical equation on the cooling zone. Flow numbers shown in this figure refer to Figure 1. By using data at flow 1 and 6, we can then solve the mathematical model simultaneously. To check the validity of the model, we have to compare the result at flow 4 and 5 with data from the plant. If their temperature and concentration of each flow are not in agreement with reference, we have to adjust correction factor \(R_f\) for temperature and \(f_k\) for concentration. There are 1 \(R_f\) and 5 \(f_k\) involved in the calculation at reduction zone. Factor \(R_f\) is differentiated...
Table 1: Reaction constants formulation for kinetic equation of iron reduction.

| Reaction                      | CO                        | H₂                        |
|-------------------------------|----------------------------|----------------------------|
| Fe₂O₃ → Fe₃O₄                 | \( k_i(\text{CO}) = 9 \cdot \exp[-49884/RT] \) | \( k_i(\text{H}_2) = 45 \cdot \exp[-49884/RT] \) |
| Fe₃O₄ → FeO                  | \( k_i(\text{CO}) = 0.072 \cdot \exp[-21616/RT] \) | \( k_i(\text{H}_2) = 0.36 \cdot \exp[-21616/RT] \) |
| FeO → Fe                     | \( k_i(\text{CO}) = 0.036 \cdot \exp[-21616/RT] \) | \( k_i(\text{H}_2) = 9 \cdot \exp[-21616/RT] \) |

Table 2: Correction factor value used in mathematical model of reduction zone.

| No. | Note                  | Methane reforming | Water gas shift reaction |
|-----|-----------------------|-------------------|--------------------------|
| (1) | Correction factor \( f \) | —                 | 0.036                    |
| (2) | Reaction constant rate \( R_f \) | *0.00199          | —                        |
| (3) | \( X \)               | 0.02              |                          |
|     | \( Y \)               | 40                |                          |
| (4) | \( Z \)               | 14800             |                          |
|     | \( V_1 \)             | 4.6E⁻⁶            |                          |
|     | \( V_2 \)             | 5.1E⁻⁶            |                          |

* Reaction constant rate (mol/m²·s·Pa⁰.⁹⁴).

based on the temperature phase, while \( f_k \) is differentiated based on kinetic equation of each reaction.

Reaction constant rate value for methane reforming is not explained in literature. The value shown in Table 2 is obtained from the calculation after fitting with the reference data.

3. Results and Discussion

3.1. Temperature, Gas, and Solid Profile along Reduction Zone.

Table 3 resumes the comparison between reference data and simulation. Reference data are taken from Project Final Report [18]. From this table, one observes that simulation precisely predicts reference data but not calculation result on the other zone. Here, root mean square error (RMSE) shows a value around 0.19. Gas composition data for flow number 1 are not available in the plant, but they can be calculated from mass balance resulted from mixing between reduction gas inlet (flow number 2) and leaking cooling gas (flow number 3). Leaking gas composition is obtained from Alamsari et al. [19].

Reduced iron data (flow number 6) at the outlet of reduction zone are also unavailable in the plant. However, the simulation results from the calculation of reduction zone already are in good agreement with simulation result produced from the calculation in isobaric zone [19]. Alamsari et al. propose model for isobaric and cooling zone of the same reactor. They found that metallization degree of the product reduces around 1.72% after leaving isobaric and cooling zone. As metallization degree of sponge iron product from the plant data is stated about 92.49%, it implies that the product (reduced iron) before entering isobaric and cooling zone has metallization degree of 94.21%. This value agrees with simulation result produced from this research. Reduced iron shown in Table 3 produces metallization degree around 94.22%. Alamsari et al. [19] also show solid temperature profile along isobaric and cooling zone. Reduced iron temperature was obtained about 1169 K. This value is close with simulation result shown in Table 3.
Reduction

\[ T^1 \rightarrow T^6 \]
\[ M^1_{\text{H}_2}, M^1_{\text{Fe}_2\text{O}_3}, M^1_{\text{Fe}_3\text{O}_4}, M^1_{\text{FeO}}, M^1_{\text{H}_2\text{O}, \text{CH}_4, \text{CO}}, M^1_{\text{N}_2}, \pi^1 \]

\[ T^6 \rightarrow \pi^6 \]

Solve momentum, mass, and energy balance equations simultaneously starting from the bottom of reduction zone

\[ T^4 \rightarrow T^5 \]
\[ M^4_i, M^5_i \]

Adjust \( R_f \)

Adjust \( f_k \)

Are \( T^4 \approx T^4_{\text{ref}} \) and \( T^5 \approx T^5_{\text{ref}} \)?

If Yes

Are \( M^4_i \approx M^4_{i,\text{ref}} \) and \( M^5_i \approx M^5_{i,\text{ref}} \)?

If Yes

Finish

Figure 4: Simulation algorithm on the reduction zone.

Figure 5: Profiles of many variables as a function of the depth of reduction zone; (a) gas and solid temperature; (b) gas concentration; (c) solid concentration.
The composition data of iron oxides are only provided for hematite (Fe$_2$O$_3$) as the main component, while the other components such as magnetite (Fe$_3$O$_4$) and wustite (FeO) are ignored because they have very small composition compared with hematite. However, since the main goal in this research is to model the whole iron reactor and kinetics equation is only small part of the model, the concentration of magnetite (Fe$_3$O$_4$) and wustite (FeO) will not affect the result.

Figure 5(a) illustrates temperature profiles along reduction zone for gas and solid phases. Inlet and outlet temperatures are in good agreement with the reference data. One observes that temperature profiles along reduction zone are increased with an increase in gas and solid temperature from the direction of solid flow. The corresponding concentration profiles for gas phase are shown in Figure 5(b). Except nitrogen, other components show composition changes which are caused by reactions in the gas phase. Gas mole balance reactions for methane reforming, iron reduction, and water gas shift reaction already have an agreement. Figure 5(c) depicts solid concentration profile along reduction zone. It is observed that, at the beginning of reduction zone inlet, total Fe in the ore is dominated by Fe$_2$O$_3$, while as reactions occur, Fe$_2$O$_3$ is slowly reduced by reduction gas to release oxygen.

3.2. Analysis the Effect of Temperature and Composition of Reduction Gas on Product Quality. Reduction gas as reactant in reduction reaction plays an important role in an enhancement of product quality. The optimum condition of reduction gas must be investigated to get the high quality. The effect of reduction gas on product quality is investigated by studying the effects of temperature and composition of reduction gas on metallization degree. The investigation is carried out by numerical simulation using the mathematical model arranged before.

3.3. Temperature. An effect of temperature on metallization degree is numerically investigated by varying inlet temperature of reduction gas on the range of 1170–1260 K with an increment around 10 K. The calculation results on reduction zone (Table 3) are used as the basis values of this simulation. The inlet temperature in this simulation is referred to as the temperature mixing of leaking cooling gas at flow 3 and reduction gas at flow 2 (see Figure 1).

Figure 6 shows the algorithm of reduction gas temperature effect on metallization degree. The calculation is started from the bottom of reduction zone. Data at flow 1 and 6 are used as input in the calculation. The simulation is carried out for each value of gas inlet temperature, and new data at flow 4 and 5 of each value are obtained. The result at flow 5 must be in good agreement with the plant data since this flow is the real input in iron reactor which is replaced by flow 6. Therefore, we have to adjust temperature ($T$) and concentration ($M$) at flow 6 until temperature ($T$) and concentration ($M$) at flow 5 agree with reference data.

Figure 7 illustrates the relation between metallization degree of reduced iron with reduction gas inlet temperature. It is observed that reduction reaction of hematite produces

![Figure 6: Simulation algorithm of reduction gas temperature effect on metallization degree of reduced iron.](image)

![Figure 7: Metallization degree as function of gas inlet temperature.](image)
higher metallization degree as an increase in reduction gas inlet temperature. This occurs because the increase in reduction gas inlet temperature causes both an enhancement of reaction temperature and an accelerate reaction flow rate. Zhang and Ostrovski [1] obtained the same result when they investigated iron ore reduction by H$_2$–CH$_4$–Ar gas mixtures. They disclose that the rate of iron ore reduction is intensified with an increase in temperature.

Although an increase in temperature can be an alternative way to get a better metallization degree, this increasing is limited by physical properties of iron. Diaz et al. [20] suggest a setting gas inlet temperature high enough to allow for liquid-phase migration of the metal iron within the pellets. However, temperature must be also maintained below the point at which the pellets became sticky. Sticky irons bring troubles because they will stimulate an agglomeration, sintered to each other and form accretions on the furnace/reactor walls. Based on the plant data, ring reduction temperature over 1153 K will initiate formation of sticky iron. It implies that reduction gas inlet temperature should be below 1246 K to avoid this problem.

3.4. Composition. In general, hydrogen and carbon monoxide are good reducers for iron ore. The change in their composition in reduction gas will affect quality of the product. Simulation of the effect of composition changes on metallization degree is performed on various composition of H$_2$ and CO. Composition of other gas is maintained on the same ratio.

Figure 8 shows the simulation algorithm of reduction gas composition effect on metallization degree of reduced iron.

Figure 9 depicts metallization degree as a function of ratio H$_2$–CO. One observes that an increase in H$_2$ composition while an attenuation of CO will produce higher metallization degree. This implies that H$_2$ is better reducer than CO. The same conclusion is reported by Bonalde et al. [2], El-Geassy and Rajakumar [3], and Pineau et al. [4]. Bonalde et al. [2] analyze metallization degree produced by using 100% H$_2$, 100% carbon monoxide, and midrex gas (55% H$_2$–34% CO) as reducer, respectively. They reported
that the fastest reaction occurs when H\textsubscript{2} is used and the slowest rate is observed when CO is used, while midrex gas is intermediate. When El-Geassy and Rajakumar [3] modeled the reduction of iron starting from wustite, they came out with the same conclusion. Pineau et al. [4] dealt with the reduction of Fe\textsubscript{2}O\textsubscript{3} in the temperature range of 220–680 °C. They found that the rate of reduction of iron oxide with H\textsubscript{2} is systematically higher than that obtained by CO.

4. Conclusions

Reduction zone of iron reactor has been simulated. Kinetics equation of reduction of hematite to iron metal, methane reforming, and water gas shift reaction are taken into account in the model. Simulation results are in good agreement with the reference data.

Temperature profiles along reduction zone show an increase in gas and solid temperature from the direction of solid flow. Gas concentration profiles show composition changes which are caused by reactions in the gas phase. Gas mole balance reaction for methane reforming, reduction, and water gas shift reaction already have an agreement.

At the beginning of reduction zone inlet, solid concentration profile shows that total Fe in the ore is dominated by Fe\textsubscript{2}O\textsubscript{3}. As reactions occur, Fe\textsubscript{2}O\textsubscript{3} is slowly reduced by reduction gas to release oxygen. Reduced iron from reduction zone produces metallization degree until 94.22%.

When an attenuation of CO yields, an increase in H\textsubscript{2} composition produces higher metallization degree. Metalization degree is also increased with an increase in gas inlet temperature. Reduction gas temperature over 1246 K is not recommended because the formation of sticky iron will be initiated.

Nomenclature

\( A_{sp} \): Pellets surface area per unit reactor volume, \( \text{m}^2/\text{m}^3 \)

\( b \): Stoichiometric coefficients

\( C \): Concentration, \( \text{mole/m}^3 \)

\( C_p \): Heat capacity, \( J/\text{moleK} \)

\( D \): Molecular diffusivity of oxygen in gas

\( D_n \): Effective diffusivity of oxygen

\( \varepsilon_p \): Pellets porosity

\( E_A \): Activation energy, \( J/\text{mole} \)

\( f \): Correction factor

\( M \): Molar flow rate, \( \text{mole/sec} \cdot \text{m}^2 \)

\( M_w \): Molecular weight, \( \text{kg/mole} \)

\( n_{pellet} \): Number of pellets per unit volume (1/m\textsuperscript{3})

\( h \): Convection heat transfer coefficient, \( \text{J/s} \cdot \text{m} \cdot \text{K} \)

\( H_{R}[298K] \): Standard reaction enthalpy, \( J/\text{mole} \)

\( k \): Preexponential constant mole \( \text{C/sec} \cdot \text{m}^3 \cdot \text{Pa} \)

\( L \): Length of reactor cooling zone, \( \text{m} \)

\( p \): Pressure, \( \text{Pa} \)

\( Q \): Flux of material, \( \text{mole/cm}^2 \cdot \text{sec} \)

\( r \): Reaction rate, \( \text{mole/m}^3 \cdot \text{sec} \)

\( R \): Gas constant, \( \text{Pa} \cdot \text{m}^3/\text{mole} \cdot \text{K} \)

\( R_c \): Radius of unreacted core, \( \text{m} \)

\( R_p \): Pellets radius, \( \text{m} \)

\( r_f \): Relaxation factor

\( T \): Temperature, \( \text{K} \)

\( \varepsilon_p \): Pore structure tortuosity

\( \varepsilon \): Superficial velocity, \( \text{m/s} \)

\( V \): Coefficients depending on weight relationships and equilibrium conditions

\( X, Y, Z \): Weight coefficients

\( z \): Space variable inside reactor, \( \text{m} \)

\( \text{solid} \): Solid

\( R \): Reaction.

Superscripts

\( + \): Forward reaction

\( - \): Backward reaction.

Subscripts

1: Reduction reaction by H\textsubscript{2}

2: Reduction reaction by CO

3: Methane reforming reaction

4: Water gas shift reaction

\( i \): \( i \)th reaction.

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