InteractE: Improving Convolution-based Knowledge Graph Embeddings by Increasing Feature Interactions

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Abstract

Most existing knowledge graphs suffer from incompleteness, which can be alleviated by inferring missing links based on known facts. One popular way to accomplish this is to generate low-dimensional embeddings of entities and relations, and use these to make inferences. ConvE, a recently proposed approach, applies convolutional filters on 2D reshapings of entity and relation embeddings in order to capture rich interactions between their components. However, the number of interactions that ConvE can capture is limited. In this paper, we analyze how increasing the number of these interactions affects link prediction performance, and utilize our observations to propose InteractE. InteractE is based on three key ideas – feature permutation, a novel feature reshaping, and circular convolution. Through extensive experiments, we find that InteractE outperforms state-of-the-art convolutional link prediction baselines on FB15k-237. Further, InteractE achieves an MRR score that is 9\%, 7.5\%, and 23\% better than ConvE on the FB15k-237, WN18RR and YAGO3-10 datasets respectively. The results validate our central hypothesis – that increasing feature interaction is beneficial to link prediction performance. We make the source code of InteractE available to encourage reproducible research.

1 Introduction

Knowledge graphs (KGs) are structured representations of facts, where nodes represent entities and edges represent relationships between them. This can be represented as a collection of triples \((s, r, o)\), each representing a relation \(r\) between a "subject-entity" \(s\) and an "object-entity" \(o\). Some real-world knowledge graphs include Freebase (Bollacker et al. 2008), WordNet (Miller 1995), YAGO (Suchanek, Kasneci, and Weikum 2007), and NELL (Mitchell et al. 2018). KGs find application in a variety of tasks, such as relation extraction (Mintz et al. 2009), Vashishth et al. 2018), question answering (Bordes, Chopra, and Weston 2014), canonicalization (Vashishth, Jain, and Talukdar 2018), recommender systems (Zhang et al. 2016), and dialog systems (Ma et al. 2015).

However, most existing KGs are incomplete (Dong et al. 2014). The task of link prediction alleviates this drawback by inferring missing facts based on the known facts in a KG. A popular approach for solving this problem involves learning a low-dimensional representation for all entities and relations and utilizing them to predict new facts. In general, most existing link prediction methods learn to embed KGs by optimizing a score function which assigns higher scores to true facts than invalid ones. These score functions can be classified as translation distance based (Bordes et al. 2013), semantic matching based (Nickel, Rosasco, and Poggio 2016), and recent works (Bickel et al. 2016) or translation distance based (Bordes et al. 2014) or semantic matching based (Nickel, Rosasco, and Poggio 2016), and recent works (Bickel et al. 2016).

Recently, neural networks have also been utilized to learn the score function (Socher et al. 2013), Ravi Shankar, Chandrahas, and Talukdar 2017)\textsuperscript{1} Dettmers et al. 2018\textsuperscript{2} Dettmers et al. 2018\textsuperscript{†}. The motivation behind these approaches is that shallow methods like TransE (Bordes et al. 2013) and DistMult (Yang et al. 2014) are limited in their expressiveness. As noted in (Dettmers et al. 2018), the only way to remedy this is to increase the size of their embeddings, which leads to an enormous increase in the number of parameters and hence limits their scalability to larger knowledge graphs.

Early Neural Networks (CNN) have the advantage of using multiple layers, thus increasing their expressive power, while at the same time remaining parameter-efficient (Dettmers et al. 2018)\textsuperscript{1} Dettmers et al. 2018\textsuperscript{2} Dettmers et al. 2018\textsuperscript{†}. They exploit these properties and propose ConvE - a model which applies convolutional filters on stacked 2D reshapings of entity and relation embeddings. Through this, they aim to increase the number of interactions between components of these embeddings.

In this paper, we conclusively establish that increasing the number of such interactions is beneficial to link prediction performance, and show that the number of interactions that ConvE can capture is limited. We propose InteractE, a novel CNN based KG embedding approach which aims to further increase the interaction between relation and entity embeddings.

Our contributions are summarized as follows:

1. We propose InteractE, a method that augments the expressive power of ConvE through three key ideas – feature permutation, "checkered" feature reshaping, and cir-
cicular convolution.

2. We provide a precise definition of an interaction, and theoretically analyze InteractE to show that it increases interactions compared to ConvE. Further, we establish a correlation between the number of heterogeneous interactions (refer to Def. 3.2) and link prediction performance.

3. Through extensive evaluation on various link prediction datasets, we demonstrate InteractE’s effectiveness (Section 5).

The source code of InteractE and datasets used in the paper have been made available at [http://github.com/malllabiisc/InteractE](http://github.com/malllabiisc/InteractE).

### 2 Related Work

**Non-Neural:** Starting with TransE (Bordes et al. 2013), there have been multiple proposed approaches that use simple operations like dot products and matrix multiplications to compute a score function. Most approaches embed entities as vectors, whereas for relations, vector (Bordes et al. 2013) [Nickel, Rosasco, and Poggio 2016], matrix (Yang et al. 2014) [Liu, Wu, and Yang 2017] and tensor (Lin et al. 2015) representations have been explored. For modeling uncertainty of learned representations, Gaussian distributions (He et al. 2015) [Xiao, Huang, and Zhu 2016] have also been utilized. Methods like TransE (Bordes et al. 2013) and TransH (Wang et al. 2014a) utilize a translati onal objective for their score function, while DistMult (Yang et al. 2014) and ComplEx (Trouillon et al. 2016) use a bilinear diagonal based model.

**Neural Network based:** Recently, Neural Network (NN) based score functions have also been proposed. Neural Tensor Network (Socher et al. 2013) combines entity and relation embeddings by a relation-specific tensor which is given as input to a non-linear hidden layer for computing the score. (Dong et al. 2014) [Ravishankar, Chandrasah, and Talukdar 2017] also utilize a Multi-Layer Perceptron for modeling the score function.

**Convolution based:** Convolutional Neural Networks (CNN) have also been employed for embedding Knowledge Graphs. ConvE (Dettmers et al. 2018) uses convolutional filters over reshaped subject and relation embeddings to compute an output vector and compares this with all other entities in the knowledge graph. [Shang et al. 2019] propose ConvTransE a variant of the ConvE score function. They eschew 2D reshaping in favor of directly applying convolution on the stacked subject and relation embeddings. Further, they propose SACN which utilizes weighted graph convolution along with ConvTransE.

ConvKB (Nguyen et al. 2018) is another convolution based method which applies convolutional filters of width 1 on the stacked subject, relation and object embeddings for computing score. As noted in (Shang et al. 2019), although ConvKB was claimed to be superior to ConvE, its performance is not consistent across different datasets and metrics. Further, there have been concerns raised about the validity of its evaluation procedure (Sun et al. 2019b). Hence, we do not compare against it in this paper. A survey of all variants of existing KG embedding techniques can be found in (Nickel et al. 2016) [Wang et al. 2017].

Most existing KG embedding approaches define an encoding for all entities and relations, i.e., $e_s, e_r \forall s \in \mathcal{E}, r \in \mathcal{R}$. Then, a score function $\psi(s, r, o)$ is defined to measure the validity of triples. Table 1 lists some of the commonly used score functions. Finally, to learn the entity and relation representations, an optimization problem is solved for maximizing the plausibility of the triples $T$ in the KG.

**ConvE:** In this paper, we build upon ConvE (Dettmers et al. 2018), which models interaction between entities and relations using 2D Convolutional Neural Networks (CNN). The score function used is defined as follows:

$$\psi(s, r, o) = f(\text{vec}(f([e_s; e_r \ast w])))W e_o,$$

where, $e_s, e_r \in \mathbb{R}^{d_w \times d_h}$, $e_o \in \mathbb{R}^{d_w \times d_h}$ denote 2D reshapings of $e_s \in \mathbb{R}^{d_w \times d_h}$, $e_r \in \mathbb{R}^{d_w \times d_h}$, and $\ast$ denotes the
convolution operation. The 2D reshaping enhances the interaction between entity and relation embeddings which has been found to be helpful for learning better representations (Nickel, Rosasco, and Poggio 2016).

3 Notation and Definitions

Let \( e_s = (a_1, ..., a_d), e_r = (b_1, ..., b_d) \), where \( a_i, b_i \in \mathbb{R} \) for all \( i \), be an entity and a relation embedding respectively, and let \( w \in \mathbb{R}^{k \times k} \) be a convolutional kernel of size \( k \). Further, we define that a matrix \( M_k \in \mathbb{R}^{k \times k} \) is a \( k \)-submatrix of another matrix \( N \in \mathbb{R}^{m \times n} \) if \( \exists i,j \) such that \( M_k = N_{i:i+k,j:j+k} \). We denote this by \( M_k \subseteq N \).

**Definition 3.1. (Reshaping Function)** A reshaping function \( \phi : \mathbb{R}^d \times \mathbb{R}^d \to \mathbb{R}^{m \times n} \) transforms embeddings \( e_s \) and \( e_r \) into a matrix \( \phi(e_s, e_r) \), where \( m \times n = 2d \). For conciseness, we abuse notation and represent \( \phi(e_s, e_r) \) by \( \phi \). We define three types of reshaping functions.

- **Stack** \( (\phi_{stk}) \) reshapes each of \( e_s \) and \( e_r \) into a matrix of shape \( (m/2) \times n \), and stacks them along their height to yield an \( m \times n \) matrix (Fig. 2a). This is the reshaping function used in (Dettmers et al. 2018).

- **Alternate** \( (\phi_{alt}) \) reshapes \( e_s \) and \( e_r \) into matrices of shape \( (m/2) \times n \), and stacks \( \tau \) rows of \( e_s \) and \( e_r \) alternately. In other words, as we decrease \( \tau \), the "frequency" with which rows of \( e_s \) and \( e_r \) alternate increases. We denote \( \phi_{alt}(\tau = 1) = \phi_{alt} \) for brevity (Fig. 2b).

- **Checkered** \( (\phi_{chk}) \) arranges \( e_s \) and \( e_r \) such that no two adjacent cells are occupied by components of the same embedding (Fig. 2c).

**Definition 3.2. (Interaction)** An interaction is defined as a triple \((x, y, M_k)\), such that \( M_k \subseteq \phi(e_s, e_r) \) is a \( k \)-submatrix of the reshaped input embeddings; \( x, y \in M_k \) and are distinct components of \( e_s \) or \( e_r \). The number of interactions \( N(\phi, k) \) is defined as the cardinality of the set of all possible triples. Note that \( \phi \) can be replaced with \( \Omega(\phi) \) for some padding function \( \Omega \).

An interaction \((x, y, M_k)\) is called **heterogeneous** if \( x \) and \( y \) are components of \( e_s \) and \( e_r \), respectively, or vice versa. Otherwise, it is called **homogeneous**. We denote the number of heterogeneous and homogeneous interactions as \( N_{\text{het}}(\phi, k) \) and \( N_{\text{homo}}(\phi, k) \) respectively. For example, in a \( 3 \times 3 \) matrix \( M_3 \), if there are 5 components of \( e_s \) and 4 of \( e_r \), then the number of heterogeneous and homogeneous interactions are: \( N_{\text{het}} = 2(5 - 4) = 10 \) and \( N_{\text{homo}} = 2 \left( \binom{3}{2} + \binom{3}{2} \right) = 12 \). Please note that the sum of total number of heterogeneous and homogeneous interactions in a reshaping function is constant and is equal to \( 2\binom{k^2}{2} \), i.e., \( N_{\text{het}}(\phi, k) + N_{\text{homo}}(\phi, k) = 2\binom{k^2}{2} \).

4 InteractE Overview

Recent works (Yang et al. 2014, Nickel, Rosasco, and Poggio 2016) have demonstrated that expressiveness of a model can be enhanced by increasing the possible interactions between embeddings. ConvE (Dettmers et al. 2018) also exploits the same principle albeit in a limited way, using convolution on 2D reshaped embeddings. InteractE extends this notion of capturing entity and relation feature interactions using the following three ideas:

- **Feature Permutation**: Instead of using one fixed order of the input, we utilize multiple permutations to capture more possible interactions.

- **Checkered Reshaping**: We substitute simple feature reshaping of ConvE with checkered reshaping and prove its superiority over other possibilities.

- **Circular Convolution**: Compared to the standard convolution, circular convolution allows to capture more feature interactions as depicted in Figure 3. The convolution is performed in a depth-wise manner (Chollet 2017) on different input permutations.

5 InteractE Details

In this section, we provide a detailed description of the various components of InteractE. The overall architecture is depicted in Fig. 4. InteractE learns a d-dimensional vector representation \((e_s, e_r \in \mathbb{R}^d)\) for each entity and relation in the knowledge graph, where \( d = d_w d_h \).
5.1 Feature Permutation

To capture a variety of heterogeneous interactions, InteractE first generates $t$-random permutations of both $e_s$ and $e_r$, denoted by $\mathcal{P}_t = \{ (e_{s,i}^t, e_{r,i}^t) : \ldots (e_{s,t}^t, e_{r,t}^t) \}$. Note that with high probability, the sets of interactions within $\phi(e_{s,i}^t, e_{r,i}^t)$ for different $i$ are disjoint. This is evident because the number of distinct interactions across all possible permutations is very large. So, for $t$ different permutations, we can expect the total number of interactions to be approximately $t$ times the number of interactions for one permutation.

5.2 Checkered Reshaping

Next, we apply the reshaping operation $\phi_{chk}(e_{s,i}^t, e_{r,i}^t), \forall i \in \{ 1, \ldots, t \}$, and define $\phi(\mathcal{P}_t) = [\phi(e_{s,1}^t, e_{r,1}^t); \ldots ; \phi(e_{s,t}^t, e_{r,t}^t)]$. ConvE (Dettmers et al. 2018) uses $\phi_{stk}(-)$ as a reshaping function which has limited interaction capturing ability. On the basis of Proposition 6.3, we choose to utilize $\phi_{chk}(-)$ as the reshaping function in InteractE, which captures maximum heterogeneous interactions between entity and relation features.

5.3 Circular Convolution

Motivated by our analysis in Proposition 6.4, InteractE uses circular convolution, which further increases interactions compared to the standard convolution. This has been successfully applied for tasks like image recognition (Wang et al. 2018). Circular convolution on a 2-dimensional input $I \in \mathbb{R}^{m \times n}$ with a filter $w \in \mathbb{R}^{k \times k}$ is defined as:

$$[I \ast w]_{p,q} = \sum_{i=-[k/2]}^{[k/2]} \sum_{j=-[k/2]}^{[k/2]} I_{p-i, q-j} \cdot w_{i,j},$$

where $[x]_n$ denotes $x$ modulo $n$ and $\lfloor \cdot \rfloor$ denotes the floor function. Figure 3 and Proposition 6.4 show how circular convolution captures more interactions compared to standard convolution with zero padding.

InteractE stacks each reshaped permutation as a separate channel. For convolving permutations, we apply circular convolution in a depth-wise manner (Chollet 2017). Although different sets of filters can be applied for each permutation, in practice we find that sharing filters across channels works better as it allows a single set of kernel weights to be trained on more input instances.

5.4 Score Function

The output of each circular convolution is flattened and concatenated into a vector. InteractE then projects this vector to the embedding space ($\mathbb{R}^d$). Formally, the score function used in InteractE is defined as follows:

$$\psi(s, r, o) = g(\text{vec}(f(\phi(\mathcal{P}_k) \oplus w))W)e_o,$$

where $\oplus$ denotes depth-wise circular convolution, $\text{vec}(\cdot)$ denotes vector concatenation, $e_o$ represents the object entity embedding matrix and $W$ is a learnable weight matrix. Functions $f$ and $g$ are chosen to be ReLU and sigmoid respectively. For training, we use the standard binary cross entropy loss with label smoothing.

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6 Theoretical Analysis

In this section, we analyze multiple variants of 2D reshaping with respect to the number of interactions they induce. We also examine the advantages of using circular padded convolution over the standard convolution.

For simplicity, we restrict our analysis to the case where the output of the reshaping function is a square matrix, i.e., $m = n$. Note that our results can be extended to the general case as well. Proofs of all propositions herein are included in the supplementary material.

**Proposition 6.1.** For any kernel $w$ of size $k$, for all $n \geq \left(\frac{2k}{\tau'} - 1\right)$ if $k$ is odd and $n \geq \left(\frac{2k+2}{\tau' \tau} - 1\right)$ if $k$ is even, the following statement holds:

$$N_{\text{het}}(\phi_{alt}, k) \geq N_{\text{het}}(\phi_{stk}, k)$$

**Proposition 6.2.** For any kernel $w$ of size $k$ and for all $\tau < \tau'$ ($\tau, \tau' \in \mathbb{N}$), the following statement holds:

$$N_{\text{het}}(\phi^\tau_{alt}, k) \geq N_{\text{het}}(\phi^\tau'_{alt}, k)$$

**Proposition 6.3.** For any kernel $w$ of size $k$ and for all reshaping functions $\phi : \mathbb{R}^d \times \mathbb{R}^d \rightarrow \mathbb{R}^{n \times n}$, the following statement holds:

$$N_{\text{het}}(\phi_{chk}, k) \geq N_{\text{het}}(\phi, k)$$

**Proposition 6.4.** Let $\Omega_0, \Omega_e : \mathbb{R}^{n \times n} \rightarrow \mathbb{R}^{(n+p) \times (n+p)}$ denote zero padding and circular padding functions respectively, for some $p > 0$. Then for any reshaping function $\phi$, $N_{\text{het}}(\Omega_e(\phi), k) \geq N_{\text{het}}(\Omega_0(\phi), k)$

7 Experimental Setup

7.1 Datasets

In our experiments, following (Dettmers et al. 2018; Sun et al. 2019a), we evaluate on the three most commonly used link prediction datasets. A summary statistics of the datasets is presented in Table 3.

- FB15k-237 (Toutanova and Chen 2015) is a improved version of FB15k (Bordes et al. 2013) dataset where all inverse relations are deleted to prevent direct inference of test triples by reversing training triples.
Table 2: Link prediction results of several models evaluated on FB15k-237, WN18RR and YAGO3-10. We find that InteractE outperforms all other methods across metrics on FB15k-237 and in 3 out of 4 settings on YAGO3-10. Since InteractE generalizes ConvE, we highlight performance comparison between the two methods specifically in the table above. Please refer to Section 8.1 for more details.

- **WN18RR** (Dettmers et al. 2018) is a subset of WN18 (Bordes et al. 2013) derived from WordNet (Miller 1995), with deleted inverse relations similar to FB15k-237.
- **YAGO3-10** is a subset of YAGO3 (Suchanek, Kasneci, and Weikum 2007) constitutes entities with at least 10 relations. Triples consist of descriptive attributes of people.

### 7.2 Evaluation protocol

Following (Bordes et al. 2013), we use the filtered setting, i.e., while evaluating on test triples, we filter out all the valid triples from the candidate set, which is generated by either corrupting the head or tail entity of a triple. The performance is reported on the standard evaluation metrics: Mean Reciprocal Rank (MRR), Mean Rank (MR) and Hits@1, and Hits@10. We report average results across 5 runs. We note that the variance is substantially low on all the metrics and hence omit it.

### 7.3 Baselines

In our experiments, we compare InteractE against a variety of baselines which can be categorized as:

- **Non-neural**: Methods that use simple vector based operations for computing score. For instance, DistMult (Yang et al. 2014), ComplEx (Trouillon et al. 2016), KBGAN (Cai and Wang 2018), KBLRN (García-Durán and Niepert 2018) and RotatE (Sun et al. 2019a).

- **Neural**: Methods which leverage a non-linear neural network based architecture in their scoring function. This includes R-GCN (Schlichtkrull et al. 2017), ConvE (Dettmers et al. 2018), ConvTransE (Shang et al. 2019), and SACN (Shang et al. 2019).

### 8 Results

In this section, we attempt to answer the questions below:

Q1. How does InteractE perform in comparison to the existing approaches? (Section 8.1)

Q2. What is the effect of different feature reshaping and circular convolution on link prediction performance? (Section 8.2)

Q3. How does the performance of our model vary with number of feature permutations? (Section 8.3)

Q4. What is the performance of InteractE on different relation types? (Section 8.4)
8.2 Effect of Feature Reshaping and Circular Convolution

In this section, we empirically test the effectiveness of different reshaping techniques we analyzed in Section 6. For this, we evaluate different variants of InteractE on validation data of FB15k-237 and WN18RR with the number of feature permutations set to 1. We omit the analysis on YAGO3-10 given its large size. The results are summarized in Figure 4. We find that the performance with Stacked reshaping is the worst, and it improves when we replace it with alternate reshaping. This observation is consistent with our findings in Proposition 6.1. Further, we find that MRR improves on decreasing the value of \( \tau \) in alternate reshaping, which empirically validates Proposition 6.2. Finally, we observe that checkered reshaping gives the best performance across all reshaping functions for most scenarios, thus justifying Proposition 6.3.

We also compare the impact of using circular and standard convolution on link prediction performance. The MRR scores are reported in Figure 4. The results show that circular convolution is consistently better than the standard convolution. This also verifies our statement in Proposition 6.4. Overall, we find that increasing interaction helps improve performance on the link prediction task, thus validating the central thesis of our paper.

8.3 Effect of Feature Permutations

In this section, we analyze the effect of increasing the number of feature permutations on InteractE’s performance on validation data of FB15k-237, WN18RR, and YAGO3-10. The overall results are summarized in Figure 5. We observe that on increasing the number of permutations although on FB15k-237, MRR remains the same, it improves on WN18RR and YAGO3-10 datasets. However, it degrades as the number of permutations is increased beyond a certain limit. We hypothesize that this is due to over-parameterization of the model. Moreover, since the number of relevant interactions is finite, increasing the number of permutations could become redundant beyond a limit.

8.4 Evaluation on different Relation Types

In this section, we analyze the performance of InteractE on different relation categories of FB15k-237. We chose FB15k-237 for analysis over other datasets because of its
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[Lin et al. 2015] Lin, Y.; Liu, Z.; Sun, M.; Liu, Y.; and Zhu, more and diverse set of relations. Following (Wang et al. 2014b), we classify the relations based on the average number of tails per head and heads per tail into four categories: one-to-one, one-to-many, many-to-one, and many-to-many. The results are presented in Table 4. Overall, we find that InteractE is effective at modeling complex relation types like one-to-many and many-to-many whereas, RotatE captures simple relations like one-to-one better. This demonstrates that an increase in interaction allows the model to capture more complex relationships.

9 Conclusion

In this paper, we propose InteractE, a novel knowledge graph embedding method which alleviates the limitations of ConvE by capturing additional heterogeneous feature interactions. InteractE is able to achieve this by utilizing three central ideas, namely feature permutation, checkered feature reshaping, and circular convolution. Through extensive experiments, we demonstrate that InteractE achieves a consistent improvement on link prediction performance on multiple datasets. We also theoretically analyze the effectiveness of the components of InteractE, and provide empirical validation of our hypothesis that increasing heterogeneous feature interaction is beneficial for link prediction with ConvE. This work demonstrates a possible scope for improving existing knowledge graph embedding methods by leveraging rich heterogenous interactions.

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Table 4: Link prediction results by relation category on FB15k-237 dataset for RotatE, ConvE, and InteractE. Following (Wang et al., 2014b), the relations are categorized into one-to-one (1-1), one-to-many (1-N), many-to-one (N-1), and many-to-many (N-N). We observe that InteractE is effective at capturing complex relations compared to RotatE. Refer to Section B.4 for details.
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