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An Ultra-Reliable Low-Latency Non-Binary Polar Coded SCMA Scheme

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Abstract—The joint transmission scheme of polar codes and sparse code multiple access (SCMA) has been regarded as a promising technology for future wireless communication systems. However, most of the existing polar-coded SCMA (PC-SCMA) systems suffer from high latency caused by the feedback iteration and list decoding. In addition, the error performance of PC-SCMA systems is unsatisfactory for ultra-reliable transmission. Inspired by the compelling benefits of non-binary polar codes, in this paper, we design a non-binary polar-coded SCMA (NB-PC-SCMA) system with a free order matching strategy to address the issues of delay and reliability. Specifically, we first formulate a joint factor graph for NB-PC-SCMA and propose a non-binary successive cancellation list (NB-SCL) and damping based joint iterative detection and decoding (NSD-JIDD) multiuser receiver to improve the BER and latency performance. Then, a lazy-search based NB-SCL (L-NB-SCL) decoding is proposed to reduce the computational complexity by simplifying the path search pattern of the list decoder. After that, we modify the update of user nodes for SCMA detection to improve the convergence error and finally propose the improved NSD-JIDD (ISD-JIDD) algorithm, which can avoid redundant operations by exploiting L-NB-SCL decoding. Simulation results show that the proposed NB-PC-SCMA system achieves better bit error rate (BER) performance and considerable latency gain when compared to its counterparts. In particular, the proposed ISD-JIDD can achieve similar BER performance of NSD-JIDD with less complexity.

Index Terms—Polar Codes, SCMA, Ultra-Reliable Low-Latency Communication, Multiuser Receiver, Joint Iterative Detection and Decoding.

I. INTRODUCTION

With the rapid development of wireless communication networks, improving the spectrum efficiency with limited physical resources has become an urgent call for 5G/6G communication systems. One of the key technologies to solve this problem is the non-orthogonal multiple access (NOMA) scheme [1]. Sparse code multiple access (SCMA), a potent code-domain NOMA scheme, is a new candidate for future communication systems attributed to the superior capacity of overload tolerance and resource reuse [2]. At the receiver end, the message passing algorithm (MPA) is adopted to detect individual user symbols.

However, the SCMA system still fails to meet the throughput and reliability for future networks [3]. In [4], the amalgamation with existing techniques, e.g., channel coding, was introduced to improve the performance of SCMA. So far, turbo coded SCMA (TC-SCMA) [5]–[7] and low-density parity-check (LDPC) coded SCMA (LDPC-SCMA) [8]–[11] systems have been widely investigated to obtain a coding gain. While these works conceived impressive joint detection and decoding (JDD) algorithms based on “turbo principle” for co-design systems, the above coding schemes are difficult to meet the ultra-reliable transmission for future communication systems and suffer a high computational complexity.

As a standard code for control channels for 5G New Radio (URLLC) [26] for future wireless networks.

Benefiting from the above achievements, polar-coded SCMA (PC-SCMA) systems have been investigated in the literature. A typical JDD scheme directly combines soft-input soft-output polar decoder and SCMA detector [12]–[16]. Specifically, the authors in [12] proposed a JDD algorithm amalgamating MPA with belief propagation decoding to obtain performance gains. As a further development, a joint iteration detection and decoding (JIDD) receiver using a soft cancellation (SCAN) decoder was proposed in [13] without inner iteration, which laid a foundation for JDD-based PC-SCMA receivers. In [14]–[16], some modified versions of JIDD were proposed to accelerate the convergence and reduce the computational complexity. However, none of these traditional soft-input soft-output schemes can break the BER performance limit of the SCAN decoder.

In contrast, an alternative JDD scheme amalgamates the soft-input hard-output polar decoder with the SCMA detector [17]–[23]. To be more specific, a sequential user partition based JDD receiver was proposed in [17], [18] with limited receiver performance due to the feedback of hard outputs. The authors in [19] first proposed a JDD scheme using
a soft-input soft-output based successive cancellation (SC) decoder to achieve performance gains. Furthermore, a JIDD employing an SC-list (SCL) decoder was presented in [20], [21], which shows a better BER performance by designing the SCL decoder’s extrinsic messages for turbo iteration. A joint channel estimation and detection scheme was also proposed for fading channels [22], [23].

However, most of the soft-input hard-output schemes still lag behind the latency and BER target of URLLC. As a promising solution, non-binary polar codes (NB-PCs) can polarize discrete memoryless channels with arbitrary $q$-ary alphabets for ultra-reliable transmission [27]. Importantly, NB-PCs can save decoding latency by symbol-level operation instead of bit-level counterparts [28], providing potential for URLLC application. Moreover, NB-PCs with different non-binary kernels over $GF(q)$ were investigated in [29]–[31], which shows significant BER gains over binary counterparts.

The existing studies on coded SCMA systems employing JDD are summarized in Table I, which facilitates a comparison of this paper’s contributions with other state-of-the-art research. As can be observed, these studies have mainly focused on BER improvement and complexity reduction, while there is a scarcity of literature on latency reduction, overload impact, early termination (ET), damping techniques and non-binary coding. Note that none of these work jointly designed coded SCMA systems are hopefully improved with NB-PCs, the receiver suffers an increased decoding complexity, which is unfriendly for hardware implementation. As a result, the receiver also requires a latency reduction technique.

In this paper, we are engaged in tackling the above challenges to investigate the NB-PC-SCMA system. The main contributions of this paper are outlined as follows.

1) To the best of our knowledge, it is the first time to propose an NB-PC-SCMA scheme with free order matching strategy (FOMS). Specifically, we introduce symbol-to-bit conversion at the transmitter while the receiver applies a novel information exchange rule among the bits, field symbols, and SCMA codewords. With the aid of FOMS, the proposed system can freely select the field and modulation order configurations according to the requirements without the limitation of the NB-PC alphabet size.

2) Furthermore, we propose a non-binary SCL (NB-SCL) and damping based JIDD (NSD-JIDD) algorithm for NB-PC-SCMA systems by combining the factor graphs of the NB-PC decoder and the SCMA detector into a joint factor graph (JFG). According to the connection in the JFG, the extrinsic soft information is exchanged and is compressed by damping techniques to improve error propagation. In addition, a cyclic redundancy check (CRC)-based ET is applied to eliminate redundant iterations, which facilitates clock cycle savings for the receiver.

3) To reduce the complexity of the iterative receiver and enhance the convergence performance, the receiver constituents, i.e., the SCMA detector and the polar decoder, are improved. A lazy-search based NB-SCL (L-NB-SCL) decoding is proposed to avoid redundant path splitting.
Table II
Summary of abbreviations.

| Acronyms | Full Form | Acronyms | Full Form |
|----------|-----------|----------|-----------|
| AWGN     | additive white gaussian noise | NB-LDPC-SCMA | NB-LDPC coded SCMA |
| BER      | bit error rate | NB-PC | non-binary polar code |
| COMS     | constrained order matching strategy | NB-PC-SCMA | non-binary PC-SCMA |
| CRC      | cyclic redundancy check | NB-SCL | non-binary SCL |
| ET       | early termination | NSD-JIDD | NB-SCL and damping based JIDD |
| FOMS     | free order matching strategy | ISD-JIDD | improved NSD-JIDD |
| IN       | intermediate node | PC-SCMA | polar-coded SCMA |
| JDD      | joint detection and decoding | PN | polar node |
| JFG      | joint factor graph | RN | resource node |
| JIDD     | joint iteration detection and decoding | SC | successive cancellation |
| LDPC     | low-density parity-check | SCAN | soft cancellation |
| LDPC-SCMA | LDPC coded SCMA | SCL | SC-list |
| LLR      | log-likelihood ratio | SCMA | sparse code multiple access |
| L-NB-SCL | lazy-search based NB-SCL | TC-SCMA | turbo coded SCMA |
| MPA      | message passing algorithm | UN | user nodes |
| NB-LDPC  | non-binary LDPC | ULLLC | ultra-reliable low-latency communication |

in the decoding process. In addition, update operations that are less dominant for user nodes are removed in the SCMA detection process to make full use of the a priori information. Accordingly, the resultant improved NSD-JIDD (ISD-JIDD) algorithm can significantly decrease the computational complexity in the receiver.

The rest of this paper is organized as follows. Section II presents the FOMS and the proposed NB-PC-SCMA system model. Following this, a multiuser iterative receiver is designed in Section III, while its improved scheme is detailed in Section IV. Section V discusses the performance of our proposed system over BER, complexity, and latency with numerical simulation results. Finally, the conclusions and future research prospects are drawn in Section VI. Especially, the key abbreviations employed in this paper are summarized in Table II for ease of access.

II. SYSTEM MODEL

A. Free Order Matching Strategy

Assume that $q$-ary codewords are converted into symbols by $M$-point SCMA modulation at the transmitter. Fig. 1 exemplifies the difference between COMS and FOMS under non-binary coded SCMA systems. For COMS of $q = 16$ shown in Fig. 1(a), every four bits are mapped into an SCMA codeword and Galois field symbol. Thus, SCMA codewords and field symbols are a group of one-to-one mapping. When $M = 4$ and $q = 16$, e.g., the case FOMS with $M < q$ in Fig. 1(b), a field symbol and an SCMA codeword are associated with 4 bits and 2 bits, respectively. In terms of field symbols, one symbol is mapped into two codewords. FOMS splits a field symbol into two sub-symbols using bit mapping. For $M = 16$ and $q = 4$, e.g., the FOMS with $M > q$ in Fig. 1(c), which is a typical multiple-to-one mapping, two field symbols are mapped into one codeword.

For COMS, only the system with $M = q$ is considered, which facilitates the modulation at the transmitter and the detection at the receiver. However, as the SCMA modulation order $M$ increases with $q$, the receiver is more prone to misjudgment and has a worse convergence speed [32]. Moreover, the system may suffer additional overhead due to the design of a large codebook.

Intuitively, COMS can be understood as a special case of FOMS with $M = q$. For FOMS, we introduce bit mapping at the transmitter, which makes adopting binary codewords for modulation feasible. Since the order matching is not limited, the universality is the visible advantage of FOMS. Importantly, the FOMS can trade-off the system throughput and reliability given the field order $q$ or SCMA modulation order $M$ according to the scene, which is demonstrated in Section V-A. The message exchange for FOMS-based receiver is depicted in Sections III.

B. System Model for FOMS Based NB-PC-SCMA

The uplink NB-PC-SCMA system with FOMS is shown in Fig. 2. The data of $J$ users are multiplexed on $K$ orthogonal resources, giving an overload factor of $\lambda = J/K$. To be more specific, the $A$-length information bits sent by user $j$ $(1 \leq j \leq J)$ are denoted as $u_j = [u_{j,1}, u_{j,2}, \ldots, u_{j,A}]$, which is encoded as $b_j = [b_{j,1}, b_{j,2}, \ldots, b_{j,D}]$ by CRC encoder. The bits in $b_j$ are converted to the field symbol over $GF(q)$ as the $D'$-length uncoded vector $b'_j = [b'_{j,1}, b'_{j,2}, \ldots, b'_{j,D'}]$, where field size $q = 2^p$ and length $D' = D/p$. Then, $b'_j$ are placed at $D'$ information symbol positions of sequence.
\( a'_j = [a'_{j,1}, a'_{j,2}, \cdots, a'_{j,N}] \), which are determined by Monte-Carlo simulation. The remaining positions are filled with the 0-valued frozen symbols. The resultant sequence \( a'_j \) is then encoded into \( c'_j \) containing \( N' = 2^e \) symbols by the non-binary polar encoder, which can be expressed as

\[
\begin{align*}
\mathbf{c}'_j &= \mathbf{a}'_j \mathbf{G}_2 \otimes \omega, \\
\end{align*}
\]

where \( \mathbf{G}_2 \otimes \omega \) is the generator matrix of NB-PC and \( \otimes \) denotes the Kronecker product. According to [33], the kernel \( \mathbf{G}_2 \) can be represented by a \( K \times 1 \) diagonal matrix. Note that \( \mathbf{G}_2 \) contains the subcarrier if and only if the element \( \mathbf{G}_2 \) in the \( k \)-th row and \( j \)-th column of \( \mathbf{F} \) is 1. To be more specific, each user’s data is assigned to \( d_u \) (\( d_u \ll K \)) resources, while \( d_r \) (\( d_r \ll J \)) users collide over the \( k \)-th resource. The factor graph corresponding to the indicator matrix in (3) is shown in Fig. 3. There are generally two types of nodes in a factor graph, i.e., user nodes (UNs) and resource nodes (RNs). Let UN-\( j \) (\( 1 \leq j \leq J \)) and RN-\( k \) (\( 1 \leq k \leq K \)) denote the \( j \)-th UN and the \( k \)-th RN, respectively.

Here, we assume that all users are time-synchronized and thus the \( e \)-th received signal is the superposition of all users’ signals, which can be expressed as

\[
y_e = \sum_{j=1}^{J} \text{diag}(\mathbf{h}_{j,e}) \mathbf{x}_{j,e} + \mathbf{z}_e, 
\]

where \( \mathbf{y}_e = \left[ y_{1,e}^T, y_{2,e}^T, \cdots, y_{E,e}^T \right]^T \) is the received signal, \( \mathbf{h}_{j,e} = \left[ h_{j,e,1}, h_{j,e,2}, \cdots, h_{j,e,K} \right]^T \) is the channel gain vector and \( \mathbf{z}_e \) is the \( K \times 1 \) additive Gaussian vector with element-wise 0 mean and covariance matrix \( \mathbf{N}_0 \mathbf{I}_K \). Here, \( \mathbf{I}_K \) denotes the \( K \times K \) diagonal matrix. Note that \( h_{j, e, k} \) in \( \mathbf{h}_{j,e} \) denotes the channel gain of the \( e \)-th transmitted codeword between resource \( k \) and user \( j \), which is available to both transmitter and receiver with the assumption of perfect channel state information. Finally, all received signals in a transmission block can be represented as \( \mathbf{Y} = \left[ y_1, y_2, \cdots, y_E \right]^T \).

![Fig. 2. FOMS based NB-PC-SCMA system.](image)

![Fig. 3. SCMA factor graph for 6 users multiplexed over 4 resources.](image)

### III. Multiuser Iterative Receiver Design for NB-PC-SCMA Systems

In this section, the JFG and receiver for the proposed NB-PC-SCMA system are presented.

**A. Joint Factor Graph Model for FOMS Based NB-PC-SCMA**

To visualize our proposed receiver, we first introduce the JFG of NB-PC-SCMA, since the message exchange rules...
in the receiver solely rely on the connection of the JFG. Moreover, the designed JFG equally reflects the impact of FOMS on the receiver, which corresponds to the characteristics regarding FOMS introduced in Section II-A.

Fig. 4 exemplifies the JFG with $M = 4$, $q = 16$ and $N' = 8$, where 6 users and 4 resources are considered. Since FOMS allows $M \neq q$, the symbol-level MPA and NB-SCL are carried out over $M$-ary and $q$-ary, respectively. We build the mapping norm between the SCMA detector and the polar decoder, as shown in the transformation level in Fig. 4. Note that we term the node on the side of the polar decoder receiving a priori information as the polar node (PN) and the node at the transformation level introduced by FOMS as the intermediate node (IN). Considering $J$ users and $E$ SCMA codewords, JFG consists of $J$ polar factor graphs, $E$ SCMA factor graphs and $JN$ INs. Each polar factor graph contains $N'$ PNs. Let $\mathcal{X}_{e,j}$ and $\mathcal{V}_{e,j}$ denote RN-$k$ ($1 \leq k \leq K$) and UN-$j$ ($1 \leq j \leq J$) of the $e$-th ($1 \leq e \leq E$) codeword, respectively, and let $\mathcal{P}_{n,j}$ ($1 \leq n \leq N$) and $\mathcal{P}_{n,j}'$ ($1 \leq n \leq N'$) denote the $n$-th IN and $n'$-th PN of the $j$-th user, respectively.

Here, each UN and PN is associated with 2 INs and 4 INs, respectively, according to Fig. 1(b). Specifically, each $\mathcal{V}_{e,j}$ is connected to $\mathcal{I}_{2e-1,j}$ and $\mathcal{I}_{2e,j}$, while each $\mathcal{P}_{n,j}'$ is connected to $\mathcal{I}_{4n-3,j}$, $\mathcal{I}_{4n-2,j}$, $\mathcal{I}_{4n-1,j}$, and $\mathcal{I}_{4n,j}$. Therefore, we can imagine that $\mathcal{P}_{n,j}'$ is linked to $\mathcal{V}_{2n-1,j}$ and $\mathcal{V}_{2n,j}$.

We integrate the polar factor graph and SCMA factor graph of different symbol levels into one JFG using IN, where messages are passed iteratively. Thus, the receiver for the proposed NB-PC-SCMA system only requires outer iterations, i.e., the loop of the overall operation. There is no inner iteration in the component SCMA detector or polar decoder. Note that we only give the JFG example for $M < q$. The model for $M > q$ is similar except for the connection pattern of IN. The result for $M > q$ can be easily found by referring to the interpretation for the FOMS shown in Fig. 1(c).

B. NB-SCL and Damping Based Joint Iterative Detection and Decoding

In this section, we introduce the proposed multiuser receiver for NB-PC-SCMA systems, which jointly performs SCMA detection and polar decoding. Specifically, the NSD-JIDD message passing process is exemplified in Fig. 5, which is elaborated in Sections III-B1 to III-B4.

1) SCMA Detection:

The SCMA detection process can be interpreted as message passing on the factor graph. Therefore, the connection of the factor graph can be uniquely defined by a pair of sets $\mathcal{U}(j)$ and $\mathcal{R}(k)$ as follows,

$$\mathcal{R}(k) = \{j | F_{k,j} = 1, 1 \leq j \leq J\},$$  

$$\mathcal{U}(j) = \{k | F_{k,j} = 1, 1 \leq k \leq K\}.$$  

According to the max-log-MPA method [34], in the $t$-th iteration, the messages are passed back and forth through the links in the factor graph and can be updated by (6–7). For the sake of convenience, we remove all subscripts $e$ indicating the codeword positions when describing SCMA detector since the SCMA detection operation is identical for all codewords.

For UN-$j$ ($1 \leq j \leq J$), we have

$$\xi_{j \rightarrow k}(x_{j}^{k} = w_{j,k}^{m}) = N\left(\mu^{(t-1)}(x_{j}^{k} = w_{j,k}^{m}) + \sum_{i \in \mathcal{U}(j) \setminus k} \xi_{i \rightarrow j}^{(t-1)}(x_{j}^{k} = w_{j,k}^{m})\right),$$  

while for RN-$k$ ($1 \leq k \leq K$), we have

$$\xi_{k \rightarrow j}(x_{j}^{k} = w_{j,k}^{m}) = \max_{x_{j}^{k} \in \mathcal{W}_{k,j} \cap \mathcal{R}(k)} \left\{ \psi(x_{j}^{k}) + \sum_{x_{i}^{k} \in \mathcal{W}_{i,j} \cap \mathcal{R}(k) \setminus j} \xi_{i \rightarrow k}^{(t)}(x_{i}^{k}) \right\},$$  

where $\xi_{k \rightarrow j}^{(t)}(x_{j}^{k} = w_{j,k}^{m})$ and $\xi_{j \rightarrow k}(x_{j}^{k} = w_{j,k}^{m})$ are the messages sent from RN-$k$ to UN-$j$ and from UN-$j$ to RN-$k$ in the
Then, by substituting (20) into (16), we can derive
\[ L_{ap,nb-pe}(\hat{c}_j,n) = \ln \frac{\Pr(\hat{c}_j,n = 0)}{\Pr(\hat{c}_j,n = 1)}, \quad \theta \in \mathbb{F}_q, \] (16)
where $\mathbb{F}_q$ denotes the set $\{0, 1, \alpha, \alpha^2, \ldots, \alpha^{q-2}\}$ of all elements over $GF(q)$.

**Theorem 1:** For user $j$, the $n'$-th NB-PC symbol LLR with estimate $\theta$ can be defined as
\[ L_{ap,nb-pe}(\hat{c}_j,n') = \ln \frac{\Pr(\hat{c}_j,n' = 0)}{\Pr(\hat{c}_j,n' = 1)}, \quad \theta \in \mathbb{F}_q, \] (17)
where $\mathbb{X}_\theta = [v_1, v_2, \ldots, v_p]$ is a binary row vector satisfying the mapping relationship $\{f : \mathbb{X}_\theta \to \theta\}$ over $GF(q)$ and $L_{\hat{j},n'}$ is a column vector of a priori bit LLRs, which can be written as
\[ L_{\hat{j},n'} = [L_{ap,nb-pe}(\hat{c}_{j,(n'-1)p+1}), L_{ap,nb-pe}(\hat{c}_{j,(n'-1)p+2}), \ldots, L_{ap,nb-pe}(\hat{c}_{j,n'p})]^T, \] (18)

**Proof:** Typically, the $n$-th ($1 \leq n \leq N$) a priori bit LLR of user $j$ can be defined as
\[ L_{ap,nb-pe}(\hat{c}_{j,n}) = \ln \frac{\Pr(\hat{c}_{j,n} = 0)}{\Pr(\hat{c}_{j,n} = 1)}. \] (19)

According to the connection of JFG described in Section III-A, we can conclude that $P_{n',j}$ is associated with $I_{(n'-1)p+1:j}, I_{(n'-1)p+2:j}, \ldots, I_{n'p:j}$, which implies that $\Pr(\hat{c}_{j,n'})$ can be expressed as a joint probability mass function with respect to $\Pr(\hat{c}_{j,(n'-1)p+i})$. When $\hat{c}_{j,n'} = \theta$, the function can be written as
\[ \Pr(\hat{c}_{j,n'} = \theta) = \prod_{i=1}^{p} \Pr(\hat{c}_{j,(n'-1)p+i} = v_i), \quad v_i \in \mathbb{X}_\theta. \] (20)

Then, by substituting (20) into (16), we can derive
\[ L'_{ap,nb-pe}(\hat{c}_{j,n'}) = \theta = \prod_{i=1}^{p} \ln \frac{\Pr(\hat{c}_{j,(n'-1)p+i} = 0)}{\Pr(\hat{c}_{j,(n'-1)p+i} = v_i)} = \sum_{1 \leq i \leq p, v_i \neq 0} L_{ap,nb-pe}(\hat{c}_{j,(n'-1)p+i}). \] (21)
We can find that the result of (21) is equivalent to (17).

Note that \( L'_{ap,nb-pc}(c_j',n') = 0 \) is always equal to 0 and thus does not require calculation via (17). Finally, we can obtain the all a priori symbol LLRs of user \( j \), which can be expressed as \( L'_{ap,nb-pc}(c_j') = \left[ L'_{ap,nb-pc}(c_{j,1}'), L'_{ap,nb-pc}(c_{j,2}'), \ldots, L'_{ap,nb-pc}(c_{j,N'}) \right] \). For the path metric of the NB-SCL decoder, we adjust the hardware-friendly function of the NB-PC path metric in \([35]\) to the compatible form with the LLR defined in (16). Hence, for any path \( \ell \) and level \( n' \), the path metric \( \rho_{\ell}^{(n')} \) of the NB-SCL decoder can be calculated recursively as

\[
\rho_{\ell}^{(n')} = \rho_{\ell}^{(n'-1)} + L_n'[\theta](q) - \min_{\theta \in F_q} L_n'[-\theta](q),
\]

where \( L_n'[\cdot](q) \) is the decision LLR for a given path \( \ell \), representing the LLR at the decision layer shown in Fig. 6, and \( q \in F_q \) is the \( n'\)-th estimate for the \( \ell\)-th path.

As a result, the decoded sequences with smaller path metrics can survive as candidates. Given a list size \( l \) for the NB-SCL decoder, the \( l \) most reliable paths and corresponding metrics of user \( j \) are expressed as \( A_j' = [\hat{\alpha}_{j,1}', \hat{\alpha}_{j,2}', \ldots, \hat{\alpha}_{j,l}'] \) and \( P_j = [\rho_{j,1}^{(N')}, \rho_{j,2}^{(N')}, \ldots, \rho_{j,l}^{(N')} ] \), respectively, where \( \hat{\alpha}_{j,\ell} \) and \( \rho_{j,\ell}^{(N')} \) (\( 1 \leq \ell \leq l \)) represent the \( \ell \)-th candidate symbol sequence and path metric, respectively. The codeword symbol sequences of the surviving paths are denoted as \( C_j' = [\hat{c}_{j,1}', \hat{c}_{j,2}', \ldots, \hat{c}_{j,l}'] \), i.e., the hard estimate information \( R_0 \) reaching the rightmost side, where \( \hat{c}_{j,\ell} \) is the \( \ell \)-th codeword symbol sequence. After bit mapping, we can get L candidate bit paths \( \Lambda_j = [\hat{\alpha}_{j,1}, \hat{\alpha}_{j,2}, \ldots, \hat{\alpha}_{j,l}] \) and codeword bits \( C_j = [\hat{c}_{j,1}, \hat{c}_{j,2}, \ldots, \hat{c}_{j,l}] \).

Assume that the \( \ell \)-th candidate path \( \hat{\alpha}_{j,\ell} \) can pass the CRC and show the smallest path metric. Here, if all paths fail the CRC, \( \hat{\alpha}_{j,\ell} \) only means the path with the smallest metric. Then the NB-SCL decoder outputs the parameter \( j_\ell \) for the next stage and performs the CRC check for the next user. In the last iteration, the information bits corresponding to path \( \hat{\alpha}_{j,\ell} \) are directly output as the estimated sequence \( \hat{\alpha}_{j} \) of user \( j \). The receiver performs ET and directly outputs the estimated information bits \( \hat{\alpha}_1, \hat{\alpha}_2, \ldots, \hat{\alpha}_J \) for all users if and only if the optimal path selected by each user passes the CRC.

4) Damping based Extrinsic Message Reconstruction and Prior Information Update:

Damping technique is an effective scheme to mitigate the error propagation problem and accelerate the convergence \([36]\). In this paper, we introduce a damping factor \( \varepsilon \in (0, 1] \) to compress the extrinsic message output by the polar decoder.

After NB-SCL decoding, the codeword bits \( C_j \), the corresponding path metric \( P_j \), and the index \( j_\ell \) of the selected path

\[
R_{\lambda-1}^{(n')} = R_{\lambda}^{(n')} + \gamma \cdot R_{\lambda}^{(n'+2w-l)},
\]

\[
\bar{R}_{\lambda-1}^{(n'+2w-l)} = R_{\lambda}^{(n'+2w-l)},
\]

where \( L_n'[-\theta](q) \) in \( L_n'(\cdot)(q) \) denotes the LLR with the estimated value \( \theta \), and \( \gamma \) is a Galois field element of the kernel \( G_2 \) defined in (2). Besides, \( \bar{\omega}_{\alpha} \) in (22-23) can be calculated as

\[
\bar{\omega}_{\alpha} = [\bar{\omega}_{\alpha}^1, \bar{\omega}_{\alpha}^2] = \alpha \cdot G_2,
\]
will be used for extrinsic message reconstruction. In this paper, we use the Bayes rule to calculate the likelihood information of codeword bits. The path metric $\rho_{ji}^{(N)}$ of each candidate path is first normalized to

$$\delta_{ji} = \exp \left( -\rho_{ji}^{(N)} \right) / \sum_{1 \leq j \leq J} \exp \left( -\rho_{ji}^{(N)} \right). \tag{28}$$

Then, the probability that the $n$-th ($1 \leq n \leq N$) bit takes value $\phi$ ($\phi \in \{0, 1\}$) can be obtained by

$$\Pr (\tilde{c}_{j,n} = \phi) = \sum_{1 \leq t \leq T, \phi_t = \phi} \delta_{jt}. \tag{29}$$

Therefore, the extrinsic bit LLR of the NB-SCL decoder can be written as

$$L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j,n}) = \begin{cases} -\infty & \Pr (\tilde{c}_{j,n} = 0) = 0 \\
\ln \frac{\Pr (\tilde{c}_{j,n} = 0) \Pr (\tilde{c}_{j,n} = 1)}{\Pr (\tilde{c}_{j,n} = 0) \Pr (\tilde{c}_{j,n} = 1)} & \Pr (\tilde{c}_{j,n} = 1) = 0 \\
+\infty & \Pr (\tilde{c}_{j,n} = 1) = 0 \end{cases}. \tag{30}$$

We can correct the extrinsic bit LLR of user $j$ with the selected codeword bit path $\tilde{c}_{ji}$, which can be expressed as

$$L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j,n}) = (1 - 2\delta_{ji}) \left| L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j,n}) \right|. \tag{31}$$

Before sent to the SCMA detector, the messages in the current iteration are directly damped by

$$L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j}) = \epsilon L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j}), \tag{32}$$

where $L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j})$ denotes the extrinsic message of NB-PCs in the $t$-th iteration.

Note that the extrinsic messages of SCMA are not moderated since the damping of the extrinsic messages output by MPA detectors and polar decoder lead to a similar a priori information behavior.

After the damping-aided extrinsic message reconstruction, we can obtain the extrinsic information of the polar decoder, which is then be interleaved as a priori bit LLRs of the SCMA detector as

$$L_{\text{ap}, \text{scma}} (\hat{d}_j) = \Pi \left( L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_{j}) \right). \tag{33}$$

Finally, the interleaved bit LLRs are remapped to the symbol log-likelihood of SCMA and are sent into the SCMA detector subsequently as the a priori information for the next iteration, which can be expressed as (34) by employing the Jacobi approximation.

$$\mu (x_{j,e}^k) = \sum_{s_{j,e} \in \mathcal{S}_{j,e}} \left\{ (1 - s_{j,e}) L_{\text{ap}, \text{scma}} (\hat{d}_{j,(e-1)R+r}) - \max \left[ 0, L_{\text{ap}, \text{scma}} (\hat{d}_{j,(e-1)R+r}) \right] \right\} \tag{34}$$

Note that the calculation of $\mu (x_{j,e}^k)$ in (34) is identical for all $e \in [1, K]$, which only depends on the $e$-th codeword mapped by the codebook $\mathcal{W}_j$. The proposed NSD-JIDD algorithm for the NB-PC-SCMA system is summarized in Algorithm 1.

---

**Algorithm 1**: NB-SCL and Damping Based Joint Iterative Detection and Decoding

**Input**: received signals $Y$, maximum number of iterations $T$ and damping factor $\epsilon$

**Output**: hard decisions of decoded bits $\hat{u}_1, \hat{u}_2, \cdots, \hat{u}_J$

1. **Initialization**: $\hat{c}_{j,0}^{(0)} (x_{i,j}) = 0$ and $\mu^{(0)} (x_{j,k}^k) = \log \frac{1}{N}$ for $\forall w_{j,k}^m \in \mathcal{W}_{j,k}$,

2. for $t = 1, 2, \cdots, T$ do

3. - Perform SCMA detection using (6-7) and (11);

4. - for $e = 1, 2, \cdots, E$ do

5. - for $j = 1, 2, \cdots, J$ do

6. - Calculate extrinsic bit LLRs $L_{\text{ex}, \text{scma}} (\hat{d}_j)$ of SCMA using (12);

7. - for $j = 1, 2, \cdots, J$ do

8. - De-interleave $L_{\text{ex}, \text{scma}} (\hat{d}_j)$ to obtain a priori bit LLRs $L_{\text{ap}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_j)$ of NB-PCs;

9. - for $n' \in \{1, 2, \cdots, N'\}$ do

10. - Calculate the a priori symbol LLRs $L_{\text{ap}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_j)$ of NB-PCs for $\forall \theta \in \mathbb{F}_q$

11. - using (17) to give the input of the NB-SCL decoder;

12. - Perform NB-SCL decoding for user $j$ using (22-27) to obtain $\Lambda_j, C_j$ and $P_j$;

13. - if CRC passes then

14. - Output the decoded sequences $\hat{u}_1, \hat{u}_2, \cdots, \hat{u}_J$;

15. - Break; // Activate ET

16. - for $j = 1, 2, \cdots, J$ do

17. - Perform damping based extrinsic message reconstruction using (28-32);

18. - Interleave $L_{\text{ex}, \text{nb} \rightarrow \text{pc}} (\tilde{c}_j)$ to get a priori bit LLRs $L_{\text{ap}, \text{scma}} (\hat{d}_j)$ of SCMA;

19. - for $e = 1, 2, \cdots, E$ do

20. - for $j = 1, 2, \cdots, J$ do

21. - Calculate the a priori symbol log-likelihood of SCMA employing (34);

21. Get the decoded sequences $\hat{u}_1, \hat{u}_2, \cdots, \hat{u}_J$;

---

**IV. IMPROVED SCHEME OF NSD-JIDD ALGORITHM**

In this section, we conceive an improved implementation of NSD-JIDD, namely the ISD-JIDD algorithm. To be more specific, the L-NB-SCL decoding algorithm is proposed in Section IV-A to simplify the path search pattern in NB-SCL decoding, leading to a complexity reduction. Then, in Section IV-B, we modify the UN update for SCMA detection to mitigate the convergence errors during the iterations.

**A. Lazy-Search Based NB-SCL Decoder**

Since NB-SCL decoding adopts a global optimal search strategy over $GF(q)$, the decoder searches $q$ paths at each information position, leading to redundant computation. The
During the UN update of SCMA detection, the NSD-JIDD scheme employs the SCMA a priori information from the decoder and the information passed by RN in the prior iteration. However, as another constituent of the receiver, the SCMA detector outputs unreliable likelihood information at the decoder and the information passed by RN in the prior iteration. Thus, the calculation of $l_{\text{now}} = q l_{\text{pre}}$ and $l_{\text{now}} = q^2 l_{\text{pre}}$, respectively. Then, at the next information level belonging to $B'$ (the complement of the set $B$), the search paths for both are $l_{\text{now}} = q l_{\text{pre}}$ and $l_{\text{now}} = q^2 l_{\text{pre}}$, respectively. Thus, the calculation of $(q^2-q) l_{\text{pre}}$ LLRs and path metrics are saved by L-NB-SCL decoding.

The L-NB-SCL decoding is summarized in Algorithm 2, where $R_{\lambda}(l) = [R^{(1)}_{\lambda}(l), R^{(2)}_{\lambda}(l), \ldots, R^{(N')}_{\lambda}(l)]$ (0 ≤ $\lambda$ ≤ $w$) denotes the right message of the $\lambda$-th column in the $l$-th factor graph. Note that for simplicity, the subscript $j$ representing user is omitted in Algorithm 2.

**B. Modified MPA Detection**

During the UN update of SCMA detection, the NSD-JIDD scheme employs the SCMA a priori information from the decoder and the information passed by RN in the prior iteration. However, as another constituent of the receiver, the SCMA detector outputs unreliable likelihood information at the decoder and the information passed by RN in the prior iteration. Thus, the calculation of $l_{\text{now}} = q l_{\text{pre}}$ and $l_{\text{now}} = q^2 l_{\text{pre}}$, respectively. Then, at the next information level belonging to $B'$ (the complement of the set $B$), the search paths for both are $l_{\text{now}} = q l_{\text{pre}}$ and $l_{\text{now}} = q^2 l_{\text{pre}}$, respectively. Thus, the calculation of $(q^2-q) l_{\text{pre}}$ LLRs and path metrics are saved by L-NB-SCL decoding.

The L-NB-SCL decoding is summarized in Algorithm 2, where $R_{\lambda}(l) = [R^{(1)}_{\lambda}(l), R^{(2)}_{\lambda}(l), \ldots, R^{(N')}_{\lambda}(l)]$ (0 ≤ $\lambda$ ≤ $w$) denotes the right message of the $\lambda$-th column in the $l$-th factor graph. Note that for simplicity, the subscript $j$ representing user is omitted in Algorithm 2.

**B. Modified MPA Detection**

During the UN update of SCMA detection, the NSD-JIDD scheme employs the SCMA a priori information from the decoder and the information passed by RN in the prior iteration. However, as another constituent of the receiver, the SCMA detector outputs unreliable likelihood information at

**TABLE III**

The available range of lazy search rate with different code lengths and code rates.

| $q$ | $\beta$ | $N' = 64$ | $N' = 128$ | $N' = 256$ | $N' = 512$ |
|-----|---------|-----------|-----------|-----------|-----------|
|     | $\beta_{\min}^q$ | $\beta_{\max}^q$ | $\beta_{\min}^q$ | $\beta_{\max}^q$ | $\beta_{\min}^q$ | $\beta_{\max}^q$ |
| 4   | 0.524   | 0.536     | 0.512     | 0.581     | 0.578     | 0.565     |
| 16  | 0.762   | 0.750     | 0.721     | 0.837     | 0.828     | 0.812     |

Monte Carlo simulation shows that the symbols at certain positions are completely decoded correctly. Therefore, we consider these high-reliable positions can be decided directly during decoding. In other words, we introduce a local lazy search for NB-SCL decoding. The resultant decoding algorithm, i.e., L-NB-SCL decoding, only seeks paths at unreliable positions evaluated by Monte Carlo simulations.

After the Monte Carlo simulation, let set $B$ denote the position where the decision can be achieved directly, i.e., the high-reliable position. To be more specific, $g_i$ denotes the error rate of the $i$-th (1 ≤ $i$ ≤ $N'$) symbol in the Monte Carlo simulation. Then, we define the set of lazy positions as $B = \{i\mid g_i \leq g_{th}\}$ with cardinality $|B| = \chi$, where $g_{th}$ is the selected threshold with the constraint 0 ≤ $g_{th}$ ≤ 10^{-3} (assuming 10,000 Monte Carlo simulations are performed). Naturally, set $\overline{B}$ is a subset of information position set $A$. The lazy search rate is then defined as $\beta = \chi / D'$. In particular, the lazy search rates at $g_{th} = 0$ and $g_{th} = 10^{-3}$ are denoted as $\beta_{\min}$ and $\beta_{\max}$, respectively. Therefore, we have the bound $\beta \in [\beta_{\min}, \beta_{\max}]$.

Taking the $GF(4)$ and $GF(16)$ based NB-PC as an example, Table III gives the thresholds for different code lengths $N'$ and code rates $R_c$, where Monte Carlo simulations are carried out at a signal-to-noise ratio of 2 dB. To obtain complexity reduction while maintaining performance, an appropriate $\beta$ is required to balance the trade-off between complexity and BER performance.

Different from the NB-SCL decoder, the L-NB-SCL decoder performs a lazy search, i.e., hard decision to reduce the split paths if $n' \in B$. The hard decision function for estimate $\hat{a}_{\ell,n'}$ in the $l$-th path can be expressed as

$$\hat{a}_{\ell,n'} = \arg \min_{\theta \in \mathbb{F}_q} L_{\omega}^{(n')}(\theta)_{(\ell)}.$$  \hspace{1cm} (35)

Note that if $n' \in B$, an update for the path metric is no longer required, i.e., $\rho_{\ell}^{(n')} = \rho_{\ell}^{(n'-1)}$, since the selected path complies with the SC decision, leading to a burden value of 0 in (27).

The path search process in SCL decoding can be characterized by a decoding tree. Fig. 7(a) and Fig. 7(b) show the $GF(4)$-based NB-SCL decoding tree and L-NB-SCL decoding tree, respectively. Typically, the $N'$-length $GF(q)$-based NB-PC decoding tree is a $q$-ary tree with depth $N'$. Here, the topmost root node denotes a null state and the number adjacent to each node denotes the corresponding path metric. From Fig. 7, compared with NB-SCL decoding, L-NB-SCL decoding splits only one search path when the level $n' \in B$. Generally, L-NB-SCL decoding can reach list saturation slower and avoid redundant global search.

Assume that the list is unfull with $l_{\text{pre}}$ paths surviving at the previous level. If the current stage belongs to $B$, the search paths for L-NB-SCL and NB-SCL are $l_{\text{now}} = l_{\text{pre}}$ and $l_{\text{now}} = q l_{\text{pre}}$, respectively. Then, at the next information level belonging to $B'$ (the complement of the set $B$), the search paths for both are $l_{\text{now}} = q l_{\text{pre}}$ and $l_{\text{now}} = q^2 l_{\text{pre}}$, respectively. Thus, the calculation of $(q^2-q) l_{\text{pre}}$ LLRs and path metrics are saved by L-NB-SCL decoding.

The L-NB-SCL decoding is summarized in Algorithm 2, where $R_{\lambda}(l) = [R^{(1)}_{\lambda}(l), R^{(2)}_{\lambda}(l), \ldots, R^{(N')}_{\lambda}(l)]$ (0 ≤ $\lambda$ ≤ $w$) denotes the right message of the $\lambda$-th column in the $l$-th factor graph. Note that for simplicity, the subscript $j$ representing user is omitted in Algorithm 2.
Algorithm 2: Lazy-Search Based NB-SCL Decoding

Input: maximum search width \( l \), information position set \( \mathcal{A} \), high-reliable position set \( \mathcal{B} \) and LLR initial value \( L_0 \)

Output: path metrics \( P = [\rho_1^{(N')}, \rho_2^{(N')}, \ldots, \rho_l^{(N')}] \), \( l \) bit paths \( \hat{a}_\ell = [\hat{a}_{\ell,1}, \hat{a}_{\ell,2}, \ldots, \hat{a}_{\ell,N'}] \) and codeword bits \( \hat{c}_\ell = [\hat{c}_{\ell,1}, \hat{c}_{\ell,2}, \ldots, \hat{c}_{\ell,N'}] \)

1. Initialization: \( L = \{1\}, \rho_1^{(0)} = 0 \)

for \( n' = 1, 2, \ldots, N' \) do

3. Update left message \( L_\omega^{(n')}[\eta][\ell] \) for \( \forall \ell \in L \) and \( \eta \in \mathbb{F}_q \) using (22-23);

if \( n' \notin \mathcal{A} \) then

5. \( \hat{a}_{\ell,n'} = 0 \) for \( \forall \ell \in L \);

6. Calculate the path metric \( \rho_\ell^{(n')} \) for \( \forall \ell \in L \); \( (\ell, \eta) \) using (27);

else

8. if \( n' \in \mathcal{B} \) then

9. Estimate \( \hat{a}_{\ell,n'} \) for \( \forall \ell \in L \) using (35);

10. \( \rho_\ell^{(n')} = \rho_\ell^{(n'-1)} \) for \( \forall \ell \in L \);

else

12. Calculate temporary metric \( \rho_\ell^{\text{temp}} \) for \( \forall \ell \in L \) and \( \eta \in \mathbb{F}_q \) using (27);

13. Select min \( \{l, q \mid L_l \} \) smallest \( \rho_\ell^{\text{temp}} \) and get survived symbol set \( \mathbb{Y}_\ell \) of each path;

14. for \( \ell \in L \) do

15. if \( \rho_{\ell,\eta} \) is selected then

16. \( (\hat{a}_{\ell,n'}, \rho_{\ell,\eta}) \leftarrow (\eta, \rho_{\ell,\eta}) \); \( (\ell, \eta) \)

17. if \( |\mathbb{Y}_\ell| > 1 \) then

18. for \( \theta \in \mathbb{Y}_\ell \backslash \eta \) do

19. Clone the path \( \ell \) to a new path \( \ell' \), \( \mathbb{L} \leftarrow \mathbb{L} \cup \ell' \);

20. \( (\hat{a}_{\ell',n'}, \rho_{\ell',\eta}) \leftarrow (\theta, \rho_{\ell,\theta}) \);

else

22. Kill the path \( \ell \) as \( L \leftarrow L \backslash \ell \);

23. \( R_0^{(n')}[\ell] \leftarrow \hat{a}_{\ell,n'} \);

24. Update right message employing (24-25);

for \( \ell = 1, 2, \ldots, l \) do

26. \( \hat{c}_\ell' \leftarrow R_0^{(\ell)} \);

27. Map \( \hat{a}_\ell' \) and \( \hat{c}_\ell' \) to \( \hat{a}_\ell \) and \( \hat{c}_\ell \), respectively

low \( E_b/N_0 \). To be specific, the information passed by RN commonly suffers a convergence error when \( E_b/N_0 \) is low, which leads to a BER degradation.

Explicitly, the dominant belief information passed by the UN should be the a priori information \( \mu^{(t-1)} \) in (6) since the latest a priori information from the non-binary polar decoder provides high reliability. By contrast, the passed information \( \xi^{(t-1)}_{i \rightarrow j} \) in the prior iteration is not an instant message and performs weakly at low \( E_b/N_0 \). After \( \xi^{(t-1)}_{i \rightarrow j} \) is employed to update \( L_{\text{ex}, \text{scma}} \) and \( L_{\text{ap}, \text{nb} - \text{pc}} \), the information \( \mu^{(t-1)} \) will contain the main messages in \( \xi^{(t-1)}_{i \rightarrow j} \) and will be updated again.

As such, we modify the MPA detection in NSD-JIDD by removing the second term \( \xi^{(t-1)}_{i \rightarrow j} \) in (6). In addition, the a priori information \( \mu^{(t-1)} \) is strictly normalized since \( L_{\text{ex}, \text{nb} - \text{pc}} \) is constructed by the Bayes rule. Then, the \( N^t(\cdot) \) operation can be discarded and thus save calculations. The modified UN update can be expressed as

\[
\zeta^{(t)}_{j \rightarrow k} (x^k_j = w^m_{j,k}) = \mu^{(t-1)} (x^k_j = w^m_{j,k}). \tag{36}
\]

Then, we can obtain the modified RN update rule by substituting (36) into (7) as follows,

\[
\xi^{(t)}_{k \rightarrow j} (x^k_j = w^m_{j,k}) = \max_{x^k_j \in \mathcal{W}_{j,k}, \forall i \in \mathcal{R}(k) \setminus j} \left\{ \psi (x^k_j) + \sum_{x^k_i \in \mathcal{S}_{j,k}, \forall i \in \mathcal{R}(k) \setminus j} \mu^{(t-1)} (x^k_i) \right\}. \tag{37}
\]

Therefore, the UN update in the modified MPA can be merged into the a priori information update. In this way, the ISD-JIDD does not comprise the UN update process, where the MPA detection stage can be represented by (37).

The partial message passing for NSD-JIDD and ISD-JIDD are described in Fig. 8(a) and Fig. 8(b), respectively, where the same parameters as Fig. 4 are considered. For NSD-JIDD, the messages passed by each RN are stored for the UN update in the next iteration. Whereas for ISD-JIDD, it can be interpreted that each UN integrates with \( R \) INs, instead of being stored for previous messages, which takes advantage of the updated messages promptly.

The overall steps of the ISD-JIDD algorithm are identical to the NSD-JIDD algorithm, only with the improvement...
of SCMA detection and polar decoding. Specifically, if we replace step 3 in Algorithm 1 by (37) and (11) to update the UNs and calculate soft messages, respectively, and step 11 performs the L-NB-SCL decoding in Algorithm 2, then the procedures complete the ISD-JIDD algorithm.

V. RESULTS AND DISCUSSIONS

Simulation results of the proposed NB-PC-SCMA system over additive white gaussian noise (AWGN) and Rayleigh fading channels are given and analyzed in this section. Particularly, the BER performance, computational complexity and latency are characterized in Sections V-A to V-C, respectively.

A. BER Performance

In this section, the error performance of the proposed NB-PC-SCMA system is evaluated. The SCMA codebook used in the simulation is designed according to [37]. Here, we define the $M$-dimension SCMA codebook with $J$ users and $K$ resources as $(J,K,M)$. For the receiver, the number of inner iterations for max-log-MPA detection is set to 1. NSD-JIDD and ISD-JIDD algorithms with 5 outer iterations are employed for multi-user detection. The NB-PCs transmitted over AWGN and Rayleigh fading channels are constructed by the Monte Carlo method at $E_b/N_0 = 2$ dB and $E_b/N_0 = 4$ dB, respectively, where the kernel parameter $\gamma$ is set according to [30]. Unless otherwise specified, the field order $q$ of the NB-PCs is 16. In addition, 16-CRC and 24-CRC are employed for the NB-PCs with $N = 256$ and $N = 1024$, respectively. To limit the computational complexity, the list size $l$ is set to 8.

Fig. 9(a) and Fig. 9(b) characterize the BER performance of NSD-JIDD with different $\varepsilon$ over AWGN and Rayleigh fading channels, respectively, where the codebook $(6,4,4)$ is considered. It can be seen that $\varepsilon = 0.4$ and $\varepsilon = 0.6$ achieve the best performance over AWGN and Rayleigh fading channels, respectively, and hence they are adopted for the following simulations.

Fig. 10 shows the BER comparison between FOMS and COMS over Rayleigh fading channels, where 4-point, 8-point, and 16-point SCMA modulation are considered. Here, the throughput in terms of bits per symbol [7] is defined as $\lambda R_c \log_2 M$. It can be observed that the BER performance of both COMS and FOMS degrades with the increase of throughput. Particularly, FOMS obtains 0.46 dB, 0.64 dB, and 0.97 dB gains versus COMS at the BER of $10^{-4}$ when bits per symbol are $1.5, 2.25, \text{ and } 3$, respectively. When $q = 16$, FOMS at $M = 4$ outperforms COMS at $M = 16$ about 4.23 dB at the cost of reduced throughput. Thus, we can adjust the order matching to trade-off the throughput and reliability, enabling the NB-PC-SCMA system with flexibility.

Before quantifying the performance of the ISD-JIDD algorithm for NB-PC-SCMA systems, we investigate the effect of $g_{th}$ in L-NB-SCL decoding on the BER performance in Fig. 11, where the codebook $(6,4,4)$ is considered. Note that $g_{th} = -10^{-4}$ represents the case when NB-SCL decoding is employed. We can see that within the limit of the threshold, especially at high $R_c$, there is no performance degradation when L-NB-SCL decoding is adopted at the receiver. Based on Fig. 11, we select the optimal $g_{th}$ for different configurations and calculate the corresponding $\beta$ from Monte Carlo simulation results, as shown in Table IV.

The performance comparison of ISD-JIDD and NSD-JIDD with different overloads in terms of BER and convergence are given in Fig. 12(a) and (b), respectively. For $\lambda = 150\%$, $\lambda = 200\%$, and $\lambda = 300\%$, the user number $J$ is 6, 12, and 24, respectively, where the corresponding resource number $K$
Fig. 11. The relationship between the threshold $g_{th}$ and BER of the ISD-JIDD algorithm with different $N$ and $R_c$, where $E_b/N_0$ is set to 3 dB and 5 dB for AWGN and Rayleigh fading channels when $N = 256$, respectively and where $E_b/N_0$ is set to 2.5 dB and 4.3 dB for AWGN and Rayleigh fading channels when $N = 1024$, respectively.

(a) BER performance.

(b) convergence performance.

Fig. 12. Performance comparison of ISD-JIDD and NSD-JIDD algorithms with different overloads, where $N = 256$ and $R_c = 1/2$

is 4, 6, and 8, respectively. The modulation order $M$ is set to 4. Here, the NSD-JIDD without ET and the ISD-JIDD with $\beta = 0$ are also plotted as the benchmark.

As seen in Fig. 12(a), a higher user overload $\lambda$ always leads to a poorer BER performance over both AWGN and Rayleigh fading channels despite an improved throughput. ET has no influence on the detection results at all. Moreover, ISD-JIDD shows a better performance than NSD-JIDD at low $E_b/N_0$ since ISD-JIDD avoids convergence errors with the aid of modified MPA. Overall, ISD-JIDD lags NSD-JIDD only about 0.06 to 0.09 dB at the BER of $10^{-4}$. Fig. 12(b) shows that both NSD-JIDD and ISD-JIDD require two extra iterations to converge when $\lambda = 200\%$. Apparently, the convergence performance of ISD-JIDD is not suffered, which is attributed to the ET and damping mechanisms.

Finally, we compare the BER performance of the proposed NB-PC-SCMA with ISD-JIDD to other state-of-the-art coded SCMA schemes, where the codebook $(6, 4, 4)$ is considered. To

TABLE IV

| Channel Parameters | $N = 256$ | $N = 1024$ |
|--------------------|-----------|-------------|
| $g_{th}$           | $\frac{1}{3}$ | $\frac{1}{2}$ | $\frac{2}{3}$ | $\frac{1}{3}$ | $\frac{1}{2}$ | $\frac{2}{3}$ |
| $\beta$            | 0.714     | 0.719       | 0.698        | 0.871         | 0.906        | 0.871         |

Fig. 13. BER comparison of the proposed NB-PC-SCMA to other state-of-the-art coded SCMA schemes, where $N = 256$ and $R_c = 1/2$. 
be more specific, LDPC-SCMA with JDD [8], non-binary LDPC (NB-LDPC) coded SCMA (NB-LDPC-SCMA) with joint trellis based joint decoding and detection (JTDD) [10], PC-SCMA with JIDD [13], and PC-SCMA with CRC aided joint iterative detection and SCL decoding (CAJIDS) [20] are simulated as counterparts. Especially, the PC-SCMA schemes with JIDD or CAJIDS can also be considered as benchmarks for different left-to-right strategies during polar decoding. The LDPC and NB-LDPC codes in the simulations are constructed for different left-to-right strategies during polar decoding. The simulated as counterparts. Furthermore, our proposed FOMS-based NB-PC-SCMA with $q = 16$ outperforms the COMS-based NB-LDPC-SCMA about 0.83 dB. Overall, we can find that the proposed NB-PC-SCMA system with ISD-JIDD always shows the best error correction performance.

### B. Complexity

This section evaluates the computational complexity of the receiver for the proposed NB-PC-SCMA scheme, which mainly lies in the SCMA detector and the polar decoder. Here, the computational complexity is quantified by the number of floating-point operations per second per outer iteration. Specifically, addition, multiplication, comparison, exclusive or, and exponential arithmetic operations are counted, which are represented by ADD, MUL, CMP, XOR, and EXP, respectively.

Typically, the complexity of the polar decoder is less than that of the LDPC decoder [40]. Thus, other outstanding PC-SCMA schemes, e.g., [13] and [20], are considered as comparison benchmarks. The computational complexity of different PC-SCMA schemes with various receiver strategies is presented in Table V. It can be seen that neither NSD-JIDD nor ISD-JIDD includes EXP operations since the max-log-MPA algorithm is applied. As $q$ and $N$ increase, the exponentially-growing $T_{p_1}$ leads to a high computational complexity of NSD-JIDD. By contrast, the ISD-JIDD receiver employs L-NB-SCL decoding to simplify the path search pattern, which yields a much lower complexity per outer iteration of the proposed NB-PC-SCMA system and benchmark schemes.

| Proposed NB-PC-SCMA | PC-SCMA |
|---------------------|---------|
| NSD-JIDD | ISD-JIDD | JIDD [13] | CAJIDS [20] |
| ADD | $E \left[ 2Kd_r^2 M^{d_r} + JM(d_u^2 + d_d - 1) + J \left[ (2q + 1)N\log_2 N' + 2T_{p_1} \right] \right]$ | $E Kd_r \left[ M^{d_r} (d_v + 2) - 1 \right] + 2JN\log_2 N$ | $E \left[ Kd_r \left[ M (d_u - 1) + M^{d_r} \cdot (2d_v + 4) \right] + JM (d_d - 1) \right] + JN\log_2 N$ |
| MUL | $E Kd_r \left( M^{d_r} + 2d_d + J \left[ 2 (q-1)N\log_2 N' + (q-1)T_{p_2} \right] \right)$ | $E Kd_r \left( M^{d_r} - 1 \right) + J \left[ 2 (q-1)N\log_2 N' + (q-1)T_{p_2} \right]$ | $6JN\log_2 N$ |
| CMB | $\frac{1}{2}JN\log_2 N'$ | $\frac{1}{2}JN\log_2 N'$ | $0$ |
| XOR | $0$ | $0$ | $\frac{1}{2} JN\log_2 N$ |
| EXP | $E Kd_r M^{d_r}$ | $E Kd_r M^{d_r}$ | $E Kd_r M^{d_r}$ |

| TABLE V | THE COMPUTATIONAL COMPLEXITY OF DIFFERENT PC-SCMA SCHEMES. |

The element-wise MUL of non-binary polar decoders is evaluated as ADD since such operations are represented as the addition of exponents. $T_{p_1}, T_{p_2}$ denote the number of search paths in the SCL, NB-SCL, and L-NB-SCL decoding, respectively.

Fig. 14 illustrates the computational complexity per outer iteration of the proposed NB-PC-SCMA system and benchmarks with different code lengths, where the field size $q = 4$ and the codebook $(6, 4, 4)$ are considered. We can see that when $N = 256$, NSD-JIDD yields a 48% and 36% higher...
The computational complexity per outer iteration of different PC-SCMA schemes with codebook \((6, 4, 4)\), where \(q = 4\) is considered for NB-PC-SCMA.

In comparison, the complexity of ISD-JIDD is 31% less than that of NSD-JIDD and only increases by 7% of JIDD. When \(N = 1024\), a 39% complexity reduction compared to NSD-JIDD can be observed.

C. Latency

Here, clock cycles are used to measure the latency gain of the NB-PC-SCMA system compared to the binary counterpart. Suppose that all parallelizable instructions are carried out in one clock cycle. SCMA detection takes only three cycles, i.e., each of which corresponds to RN update, UN update, and calculation of soft information. The latency of SCMA detection is negligible compared to polar decoding. Therefore, we will focus on the impact of polar decoding on the receiver latency.

The cycles of the binary SCL decoder can be calculated as

\[
\Gamma_{SCL} = 2^N - 2 + D \quad [41]
\]

with \(D\) cycles for path sorting and \(2^N - 2\) cycles for SC decoding. The latency of the SCAN decoder can be expressed as

\[
\Gamma_{SCAN} = T_{SCAN} (2^N - 2),
\]

where \(T_{SCAN}\) is the number of SCAN inner iterations. The latency of the L-NB-SCL decoder is written as

\[
\Gamma_{L-NB-SCL} = 2^N - 2 + (1 - \beta) D'.
\]

Thus, the latency for the JIDD in [13] can be expressed as

\[
\Gamma_{JIDD} = T \cdot T_{SCAN} (2^N - 2) = T (2^N - 2).
\]

According to [20], the latency for the CAJIDS can be calculated as

\[
\Gamma_{CAJIDS} = \sum_{t=1}^{T} 2N_t - 2 + D_t,
\]

where \(N_t\) and \(D_t\) denote the number of decoded bits and information bits before ET in the \(t\)-th iteration for the distributed CRC aided SCL decoding, respectively. The latency for our proposed ISD-JIDD can be expressed as

\[
\Gamma_{ISD-JIDD} = T_a (2N' - 2 + (1 - \beta) D') = \frac{T_a}{p} [2N - 2p + (1 - \beta) D],
\]

where \(T_a\) denotes the average number of iterations for the ISD-JIDD. To make a fair comparison, we employ the latency of a multiuser receiver with conventional SCL decoding as the benchmark. Then, the latency gain for algorithm \(X\) can be written as

\[
G_{latency,X} = \frac{T \cdot \Gamma_{SCL} - \Gamma_X}{T \cdot \Gamma_{SCL}},
\]

where \(\Gamma_X\) denotes the latency for a given algorithm \(X\), i.e., \(\Gamma_X \in \{\Gamma_{JIDD}, \Gamma_{CAJIDS}, \Gamma_{ISD-JIDD}\}\).

Before characterizing the latency performance, \(T_a\) versus \(E_b/N_0\) over AWGN channels is presented in Fig. 15. It can be observed that with the improvement of \(E_b/N_0\), the ET mechanism leads to a decrease of \(T_a\). Especially at \(E_b/N_0 = 5\) dB, the ISD-JIDD with \(q = 16\) converges and activates ET after 1.55 average iterations, which contrasts significantly with the maximum number of iterations \(T = 5\).

The latency gain performance for different schemes is presented in Fig. 16, where the same parameters as Fig. 13 are considered. In particular, both PC-SCMA and NB-PC-SCMA with non-iterative designs are plotted as the baseline for the iteration scheme. It can be found that for the PC-SCMA system, JIDD has a 20% latency gain regardless of \(E_b/N_0\), while CAJIDS exhibits a weak latency gain at high \(E_b/N_0\).
By contrast, for the proposed NB-PC-SCMA system, ISD-JIDD obtains about 57% to 92% latency gain, attributed to the characteristics of NB-PC, ET mechanism and L-NB-SCL decoding.

Observe also from Fig. 16 that the non-iterative scheme achieves up to 90% latency reduction since the receiver does not consider a feedback iteration mechanism. At low $E_b/N_0$, ISD-JIDD with $q = 4$ takes approximately twice the latency of the non-iterative PC-SCMA. However, the BER performance of the non-iterative system deteriorates significantly as shown in Fig. 13. Benefiting from FOMS, the latency gain of the proposed system becomes larger as $q$ increases. Note that when $E_b/N_0 = 5$ dB, a latency saving of 92% can be observed by ISD-JIDD with $q = 16$, which even outperforms that of non-iterative NB-PC-SCMA systems.

VI. CONCLUSION

In this paper, we have presented the design of the FOMS-based NB-PC-SCMA system for the first time. Specifically, an NSD-JIDD receiver has been proposed to guarantee the BER performance. Moreover, the ISD-JIDD algorithm with L-NB-SCL decoding and modified MPA have been proposed to reduce computational complexity and convergence error. Simulation results show that the proposed NB-PC-SCMA system leads to the best BER performance with up to 92% latency gain compared to other state-of-the-art architecture. Furthermore, ISD-JIDD achieve at least 31% complexity reduction over NSD-JIDD without significant BER loss. In our future work, we will extend the proposed NB-PC-SCMA scheme to the scenarios with imperfect channel state information where channel estimation technologies are considered.

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