Joint \textit{XMM-Newton} and \textit{NuSTAR} observations of the reflection spectrum of III Zw 2

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ABSTRACT

Detecting and modeling the reprocessed hard X-ray emission component in the accretion flow, the so-called reflection spectrum, is a main tool used to estimate black hole spins in a wide range of astrophysical black holes, regardless of their mass or distance. In this work, we study the X-ray spectra of the Seyfert galaxy III Zw 2 by using multiepoch \textit{XMM-Newton}, \textit{NuSTAR}, and \textit{Suzaku} observations. The X-ray spectra exhibit a soft-excess below 1 keV and a prominent excess at the location of the broad Fe Kα line at 6.4 keV. To account for these spectral features, we fit the spectra with multiple models including an ionized partially covering absorber and an accretion disk reflection model. To fully resolve the reflection component, we analyzed jointly the \textit{XMM-Newton} and \textit{NuSTAR} observations taken in 2017 and archival \textit{XMM-Newton} data from 2000. Assuming the reflection scenario, the resulting model fits support for a rapidly spinning black hole ($a \geq 0.98$) in this radio-intermediate source. The X-ray spectra in 2000 and 2017 are remarkably similar; the only difference pertains to the reflection fraction, which is possibly due to a change in the geometry of the accretion flow. However, the \textit{Suzaku} observation is markedly different, and we suggest this could be an effect of a jet contribution in the X-ray band, which is supported by the elevated radio flux during this observation.

Key words. accretion, accretion disks – black hole physics – X-rays: galaxies – galaxies: Seyfert – galaxies: active

1. Introduction

Black hole (BH) spins are fundamental physical parameters that preserve information about the formation, evolution, and the mass accretion rate history of supermassive black holes (SMBHs) residing in the centers of galaxies (Volonteri et al. 2005; Volonteri 2010). The determination of the BH spin has been addressed by three different X-ray data analysis methods (for further details see Reynolds & Fabian 2008). However, the majority of the spin measurements in active galactic nuclei (AGN) have been constrained by fitting the X-ray spectra with a model including a reprocessed (“reflected”) component from the accretion disk. The reflection spectrum encodes information about the magnitude of the spin via the location of the innermost stable circular orbit (ISCO). Currently, there are more than two dozen BH spin measurements with robust results, and a large number of them have high spin values (Reynolds 2019). Due to the clear observational features, the reflection model is one of the most preferred BH spin estimation methods. Although, some observational challenges could affect the constraining of the spin, such as obtaining a sufficiently high signal-to-noise X-ray spectrum, assessing the effect of absorption and emission features on the continuum, as well as weakness of the inner disk Fe Kα line in sources seen at low inclination angles (Laor 2019).

The magnitude of the spin of SMBHs in AGN plays an important role in constraining relativistic jet production models. Magnetic fields can extract the rotational energy of a spinning BH via the Blandford-Znajek mechanism that launches jets (Blandford & Znajek 1977). The so-called spin paradigm attempts to explain the wide radio-loudness distribution (Sikora et al. 2007) solely in terms of differences in the BH spin (Blandford 1999; Wilson & Colbert 1995; Tchekhovskoy et al. 2010). The existence of highly-spinning black holes in radio-quiet AGN does not fit well with this paradigm (e.g., Walton et al. 2013; Reynolds 2014). Hence, the production of powerful relativistic jets might not depend exclusively on high spins but also on the role of another parameter in the Blandford-Znajek mechanism, namely magnetic flux threading the black hole. For instance, Sikora & Begelman (2013) propose that the accretion history of a BH may determine whether high enough magnetic flux is accumulated in the BH to launch powerful jets. This latter model is sometimes called the “magnetic flux paradigm”. The magnetic flux, together with the BH spin determines the jet power – hence the wide range of jet powers would not only depend on the range of spins but also on the accretion history of the source. The most powerful jets, which have power that is comparable to the accretion power of the system, can be explained by the magnetically arrested disk (MAD; Narayan et al. 2003; Tchekhovskoy et al. 2011; McKinney et al. 2012) scenario in which the magnetic flux threading a BH is at the maximum value allowed by the accretion rate.

The study of the distribution of BH spins in radio-quiet and radio-intermediate AGN can potentially help to distinguish between the two paradigms. Flat-spectrum radio-intermediate quasars (RIQ) are especially interesting sources in this respect since it has been suggested that they are beamed counterparts of radio-quiet quasars (Falcke et al. 1996a,b) and since their compact radio cores, in principle, allow the jet magnetic...
Notes. The exposures shown in the table represent the total time on source.

### Table 1. X-ray observations of III Zw 2 used in this paper.

| Epoch | Mission/instrument | OBSID          | Date       | Exposure (ks) | Total counts | Energy band (keV) |
|-------|--------------------|-----------------|------------|---------------|--------------|-------------------|
| 2017  | NuSTAR: FPMA/FPMB  | 60301014002     | 2017-12-11 | 85.8/85.5     | 21212/20626  | 3–79              |
|       | XMM-Newton: EPIC-pn| 0795620101      |            | 26.2         | 203720      | 0.23–10           |
| 2011  | Suzaku: XIS0/XIS3  | 706031010       | 2011-06-14 | 65.3/65.3     | 39067/41781  | 0.7–10            |
| 2000  | XMM-Newton: EPIC-pn| 0127110201      | 2000-07-03 | 10.2         | 33264       | 0.23–10           |

**2. Observations and data reduction**

**NuSTAR** observations with the supporting **XMM-Newton** observations are currently the only set of instruments that provide the necessary sensitivity and bandpass to study the accretion processes of AGN in detail. The hard X-ray band of **NuSTAR** is used to study the reflection features of the iron line region and Compton reflection hump, and the soft X-ray band of **XMM-Newton** is used to support the study of the reflection features in the iron line region and the soft excess.

We observed III Zw 2 simultaneously with **XMM-Newton** and **NuSTAR** on December 11. In Table 1, **XMM-Newton** exposures are given for the EPIC-pn camera for the 0.2–10 keV band with a mean countrate of 8.74 ± 0.02 counts s⁻¹ (1000 s bin time). **NuSTAR** exposures are given for the two focal plane modules (FPM) in the 3–79 keV band. The mean countrates for the 7000 s bin lightcurves for both detectors are 0.590 ± 0.004 and 0.607 ± 0.004 counts s⁻¹.

**2.1. XMM-Newton**

In this work, we only analyze the EPIC-pn source spectra due to the higher sensitivity compared to the MOS cameras. The 2017 observation of III Zw 2 with the EPIC-PN camera was executed in the Prime Small window mode with a thin filter for a total duration of 41 ks and an exposure time of 26 ks. To obtain the spectra, we processed the EPIC-PN data using the HEASOFT package version 6.24 and the **XMM-Newton** Scientific Analysis System (SAS version 17.0.0) and followed the guidelines on the mission website. High-level science products were obtained using the XMMEXTRACT tool. For the light curve and spectral extraction, large background flaring was subtracted with the task TABGTIGEN by creating a good time interval file with a background countrate threshold of 0.4 count s⁻¹. No pile-up corrections were applied as the countrate during the observation is well below the small window pile-up threshold (25 count s⁻¹).

The energy band used for the spectral analysis ranges from 0.23 to 10 keV.

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1. [https://xmm-tools.cosmos.esa.int/external/xmm_user_support/documentation/sas_usg/USG/](https://xmm-tools.cosmos.esa.int/external/xmm_user_support/documentation/sas_usg/USG/)
2.2. NuSTAR

The calibration and product extraction of the NuSTAR data were performed by following the standard guidelines\(^2\). We used the NUPPIPELINE script to obtain calibrated event files for the FPMA and FPMB detectors. Subsequently, we used the NUPRODUCTS script to extract the instrumental responses, the source spectra from a 30” circular area centered on the source, and the background spectra from a 60” circular area from a source-free region. We also include the correction of South-Atlantic anomaly (SAA) effect on the background rates. The exclusion of SAA passages was carried out by using the following parameters: SAACALC = 3, SAAMODE = optimized, and TENTACLE = yes. For the spectral fitting, we used both FPM spectra in the energy range of 3–50 keV with a constant in the model to account for any differences in the normalization between the two detectors.

2.3. Archival X-ray data

In addition, we analyzed all of the available X-ray observations of III Zw 2, which were conducted in the past in comparable resolution in the soft X-ray domain, namely an XMM-Newton observation from 2000 and a Suzaku observation from 2011 (see Table 1). We reduced the XMM data of the 2000 observation similarly to the 2017 data (see above). For the Suzaku 2011 observation, we used the available data products from the XIS0 and XIS3 CCD cameras.

2.4. Radio data

The 37 GHz radio observations of III Zw 2 covering 1986–2019 were made with the 13.7 m diameter Metsähovi radio telescope in Finland (see Fig. 5, which shows the radio flux curve from 1997 to 2019). The detection limit of the telescope at 37 GHz is on the order of 0.2 Jy under optimal conditions. Data points with a signal-to-noise ratio (S/N) < 4 are handled as nondetections. The flux density scale is set by observations of DR 21. Sources NGC 7027, 3C 274, and 3C 84 are used as secondary calibrators. A detailed description of the data reduction and analysis is given in Teräsranta et al. (1998). The error estimate in the flux density includes the contribution from the measurement root mean square (rms) and the uncertainty of the absolute calibration.

3. Spectral analysis and results

This work is mainly devoted to the spectral analysis of the X-ray data by fitting models to the observed source spectra for the epochs listed in Table 1. The analysis of the X-ray spectra was performed with ISIS\(^3\) (Interactive Spectral Interpretation System, package version 1.6.2–41; Houck & Denicola 2000). Before fitting, we grouped the spectra such that each energy bin has S/N ≥ 10. The fit quality was estimated using χ^2 statistics and the uncertainties associated with the model parameters are shown at the 90% confidence level.

Figure 1 displays the X-ray spectra of III Zw 2 from the XMM-2000, Suzaku-2011, and XMM+NuSTAR-2017 observations. Overall, the spectral shape stays similar with a clear change in the flux level between the 2000 and 2017 observations. On the contrary, the Suzaku-2011 spectrum shows a change in the spectral shape with a different power-law index and stronger absorption.

We first fit the spectra with a phenomenological model, consisting of an absorbed power-law component (PHABS×POWERLAW; hereafter PL). We did not fix the value of the neutral hydrogen column density (N_H) as it was done in previous studies (Salvi et al. 2002; Jiménez-Bailón et al. 2005; Picoccelli et al. 2005; Gonzalez et al. 2018) in order to allow its possible variability over time (the Galactic value is N_H ≈ 5 × 10^{20} cm^{-2}; Kalberla et al. 2005) and to take any variability in an additional, intrinsic absorption component into account.

Figure 2a shows the data/model ratio (residuals) of the PL model in the range 0.2–10 keV for all epochs. A prominent soft X-ray excess (0.2–1 keV) is observed in the XMM-2017 spectrum similar to the 2000 data (Gonzalez et al. 2018). The existence of a soft excess in the Suzaku-2011 spectrum is difficult to ascertain due to a flatter spectrum, higher absorption, and a limited low energy response. The Suzaku-2011 spectrum appears to be significantly more absorbed with the N_H differing by a factor of at least two compared to the other epochs (see Fig. 1). Additionally, the spectrum presents a lower photon index (Γ ∼ 1.58).

A prominent excess between 5–7 keV is observed in the XMM-2000 residuals, indicating a contribution from the Fe Kα line (Salvi et al. 2002; Jiménez-Bailón et al. 2005; Gonzalez et al. 2018). Interestingly, such an excess appears to also be present in the Suzaku-2011 residuals; however, it is less prominent and statistically less significant. In contrast to these findings, the XMM+NuSTAR-2017 residuals show no significant Fe Kα line.

Based on the reduced χ^2 values shown in Table 2, it is clear that pure power-law models are not suitable to describe the XMM/NuSTAR data. Here, we point out that since the Suzaku-2011 data have a limited low energy response, they cannot be used to place any constraints on the soft excess. Thus, we conclude that the PL model can sufficiently explain the Suzaku-2011 spectrum and we do not fit any subsequent models to the data.

Secondly, we added a black body component to model the soft excess (hereafter PL+BB). The residuals of these fits for all epochs are shown in Fig. 2b. We find that PL+BB model fits the XMM+NuSTAR-2017 and the XMM-2000 data sets much better. The spectral fitting results are displayed in Table 2.

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\(^2\)https://heasarc.gsfc.nasa.gov/docs/nustar/analysis/nustar_quickstart_guide.pdf

\(^3\)https://space.mit.edu/asc/isis/docs.html
The black body temperatures of the best fitting PL+BB models range between 136 and 192 eV, which are consistent with the values reported by Piconcelli et al. (2005) and Gierliński & Done (2004). These values are much higher than the maximum temperature of the standard accretion disk (∼10 eV), which means that we cannot attribute the black body component to the thermal emission from the accretion disk. Such a large temperature of the soft excess has also been reported for several other AGN, including radio-quiet PG quasars as well as narrow line Seyfert 1 galaxies (NLS1s; Ai et al. 2010, and references therein). However, no correlation between the soft excess temperature and the black hole masses (as low as \(10^6 M_\odot\)) has been found for the large majority of the sources with the exception of radio-loud NLS1s (Yuan et al. 2010).

Above, we show that a black body-like component is needed to fit the spectrum of III Zw 2 well. The physical interpretation of the soft excess is a long-standing issue, which has been addressed by different models. These include, for instance, the Comptonization of accretion disk photons to soft X-ray energies (Ai et al. 2010, and references therein), the reflection and absorption of photons in partially ionized material (Done & Nayakshin 2007; Done et al. 2007), and magnetic reconnection on the surface of the disk accelerating nonthermal electrons, which then scatter photons via inverse Compton to soft-excess energies (Zhong & Wang 2013).

Phenomenological models including a black body component serve as a crude proxy for these physical scenarios and as such we cannot rule them out. However, individually testing a variety of such models is beyond the scope of this paper since our goal is to constrain the spin value of the central black hole in III Zw 2. In the rest of the paper, we thus concentrate on modeling the spectra within a relativistic reflection scenario that can naturally explain both the soft excess and the excess around 6.4 keV. For completeness purposes, we first shortly discuss a warm absorber model, which is a commonly proposed alternative to reflection models for explaining the observed AGN X-ray spectra.

3.1. Warm absorber model

Even if the spectra of III Zw 2 do not exhibit any strong absorption edges when compared to other sources (see Porquet et al. 2004), we also investigate a scenario where so-called warm
Fig. 3. Data-to-model ratio of (a) a power-law continuum model with partial covering of a partially ionized absorber and (b) the same as in (a), but with black body emission included.

absorber (WA; model ZXIPCF) might be present. Thus, we fit the data with a model where partially ionized absorbing material partially covers the power-law continuum source (hereafter WA*PL) as well as with the same model including a black body emitter (hereafter WA*(PL+BB)).

The results of the fits are shown in Table 2. These models produce an improvement to the fit statistics compared to the PL and PL+BB models for the XMM-2000 spectrum. While both models can effectively fit the excess around 6.4 keV, they do not fit the soft excess well (see residuals in Figs. 3a,b; bottom panels). As for the 2017 spectrum, the WA*PL model only produces a slight improvement over the PL model, and the residuals show a clear pattern in the soft X-rays similar to the PL model fit (Fig. 3a; upper panel). The WA*(PL+BB) model produces a better fit, but essentially it is very similar to the PL+BB model (with some additional reprocessing in a cool gas), so the WA cannot be the physical interpretation used to explain the soft excess in this case. The implied black-body temperature is again high and comparable to the values obtained previously without a warm absorber (see Table 2). We have also tried to fit the spectra with a power-law model modified by two warm absorbers; however, this model does not produce a significant improvement to the previous single warm absorber models fit to the 2000 spectrum, that is, we find a similar fit quality. While a double warm absorber model can improve the single warm absorber power-law fit (with $\chi^2$/d.o.f. = 589.4/458) to the 2017 spectrum, it does not fit the data above 30 keV well.

Considering that the 2000 and 2017 spectra have a similar spectral shape overall, albeit with a different X-ray flux, and that there is a sign of a broad Fe Kα line in the 2000 spectrum, we investigate a disk reflection scenario to estimate the black hole spin of III Zw 2 in the next section. As we will see, the reflection model can explain both the soft excess emission and the blurred Fe Kα line within a single physical scenario.

3.2. Reflection model

To explore physical conditions around the supermassive black hole in III Zw 2, we employed the relativistic reflection model, RELXILL\(^4\) (García et al. 2014; Dausser et al. 2014), to fit the data. RELXILL models the irradiation (in coronal geometry) of the accretion disk by an emitter with a broken power law spectrum and a radial emissivity profile. It combines the reprocessed emission from the disk with the relativistic broadening effects on the emission features. For high-quality data, the model allows for the estimation of a number of parameters, such as the disk ionization parameter ($\xi$), the iron abundance ($A_{Fe}$), the reflection fraction ($R$), the inclination angle ($\theta$), and the black hole spin ($\alpha$).

For the disk irradiation profile, we fixed the power-law indices $\beta_1 = 5$, $\beta_2 = 3$ and the break radius to $R_{br} = 4 R_g$, corresponding to a low height of the primary X-ray source from the disk (Dausser et al. 2013). The energy cutoff of the primary spectrum was set to 300 keV. Additionally, the gas density in the accretion disk is assumed to be $10^{15}$ cm\(^{-3}\) (García et al. 2016).

To constrain the spin, an assumption about the disk inclination limits has been made based on the results of previous works. It is well known that III Zw 2 has a radio jet exhibiting superluminal motion (Brunthaler et al. 2000; Lister et al. 2019). The maximum jet viewing angle of $41^\circ$ was estimated from the apparent superluminal motion by Brunthaler et al. (2000). In addition to this limit, various other estimates of the jet inclination can be derived from radio observations. Hovatta et al. (2009) reported a jet inclination angle of $35^\circ$ based on the flux variability time scale in the Metsähovi 37 GHz monitoring data and the apparent jet speed measured by the MOJAVE Survey (Lister et al. 2019). Liodakis et al. (2018) used a similar technique with the 15 GHz flux variability data from the Owens Valley Radio Observatory monitoring program and report a jet inclination angle of $22.1^\circ$ with lower and upper limits of $0.9^\circ$ and $23.5^\circ$, respectively. Furthermore, the one-sidedness of the jet in III Zw 2 can be used to place an upper limit of $53^\circ$ on the jet inclination based on the required ratio of the Doppler boosting factors for the jet and the counter-jet\(^5\). Taken together, the upper

\(^4\) http://www.sternwarte.uni-erlangen.de/~dauser/research/relxill/

\(^5\) In 2004.4, there was an ejection of a new jet emission feature that had a speed of $\beta_{app} \approx 1.36$ (Lister et al. 2019). This jet feature is well-separated from the core in the MOJAVE 15 GHz VLBA image taken on August 9, 2007. We measured the surface brightness ratio between the approaching jet and the counter-jet at a distance of 1.2 mas from the VLBI core. Since there is no detectable emission on the counter-jet side, we used three times the image’s rms noise of 0.23 mJy beam\(^{-1}\) as an upper limit. The resulting lower limit of the brightness ratio $R_g$ is 64 and the corresponding upper limit of the jet inclination is $\theta < \arccot(\frac{0.23}{64 \times 0.23}) \approx 53^\circ$, where $k = 3$ for a transient jet feature and spectral index $\alpha$ is assumed to have the canonical value of $-0.7$. 

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The fits shown in this table were performed separately for the 2000 and 2017 data sets. The fixed parameters in the model are $A_{172}$, page 6 of 11.

...values that were produced by either the relxill and relxilllp (i.e., lamp-post) model parameters.

| Model    | Model parameter | XMM-2000 | Joint XMM+NuSTAR 2017 |
|----------|----------------|----------|-----------------------|
| RELXILL  | $N_H$          | 0.097$^{+0.012}_{-0.016}$ | 0.102$^{+0.005}_{-0.003}$ |
|          | Normalization $\times 10^{-5}$ | 3.44$^{+1.06}_{-0.76}$ | 8.15$^{+0.25}_{-0.46}$ |
|          | $\Gamma$       | 1.74$^{+0.05}_{-0.06}$ | 1.87$^{+0.01}_{-0.01}$ |
|          | Total flux  $(a)$ | 7.54 | 18.3/9.2 |
|          | $a$            | $\geq 0.78$ | $\geq 0.98$ |
|          | $\theta$ $(b)$ | $38^{+3}_{-15}$ | $41^{+10}_{-1.5}$ |
|          | log($\xi$)     | 2.75$^{+0.27}_{-0.27}$ | 2.70$^{+0.06}_{-0.06}$ |
|          | $A_{Fe}$ (Solar) | 2.51$^{+0.96}_{-1.44}$ | 2.11$^{+0.53}_{-0.69}$ |
|          | $R$            | 0.81$^{+0.41}_{-0.41}$ | 0.49$^{+0.06}_{-0.05}$ |
| RELXILL_LP | $\chi^2$/d.o.f. | 136.7/134 (1.02) | 557.7/459 (1.21) |

| $N_H$    | 0.089$^{+0.011}_{-0.011}$ | 0.098$^{+0.003}_{-0.003}$ |
| Normalization $\times 10^{-4}$ | 2.21$^{+0.65}_{-1.05}$ | 5.00$^{+0.10}_{-0.07}$ |
| $\Gamma$ | 1.71$^{+0.03}_{-0.04}$ | 1.86$^{+0.01}_{-0.01}$ |
| Total flux  $(a)$ | 7.49 | 19.3/9.8 |
| $a$            | $\geq 0.64$ | $\geq 0.97$ |
| $\theta$ $(b)$ | $38^{+3}_{-15}$ | $41^{+10}_{-1.5}$ |
| log($\xi$)     | 2.77$^{+0.18}_{-0.17}$ | 2.70$^{+0.02}_{-0.05}$ |
| $A_{Fe}$ (Solar) | 3.07$^{+0.78}_{-1.75}$ | 1.66$^{+0.62}_{-0.51}$ |
| $h$ $(c)$      | $\leq 4.6$ | 3 |
| $\chi^2$/d.o.f. | 137.3/133 (1.03) | 587.6/458 (1.28) |

**Notes.** The fits shown in this table were performed separately for the 2000 and 2017 data sets. The fixed parameters in the model are $\beta_1 = 5$, $\beta_2 = 3$, $R_{in} = 4$ $R_g$, $R_{out} = 1$ ($R_{GCD}$), and $R_{out} = 400 R_g$ (see text for details). $N_H$ is given in units of $10^{23} \text{cm}^{-2}$, the power law normalization factor with the units of photons keV$^{-1}$ cm$^{-2}$ s$^{-1}$ at 1 keV, the total flux for each energy range in units of $10^{-11} \text{erg}{cm}^{-2} \text{s}^{-1}$, $\xi$ in units of erg cm s$^{-1}$, $A_{Fe}$ in solar units, and $h$ in $R_g$. $^{(a)}$Absorption-corrected fluxes were estimated for the following ranges: 0.23–10 keV (2000) and 0.7–10 keV (2017). For the latter, the total flux is the average of the XIS cameras. For the 2017 spectrum, separate calculations were made for the ranges: 0.23–10 keV (XMM) and 0.7–50 keV (NuSTAR). The total flux of the 3–50 keV range is the average value of the FPM detectors. $^{(b)}$The maximum disk inclination angle was set to 41°. $^{(c)}$The minimum default value for the height is 3 $R_g$.

limit of 41° for the jet inclination appears well-motivated. We assume that the jet is launched perpendicular to the accretion disk and, thus, we also set the maximum limit for the disk inclination to 41°.

We first fit the 2000 and 2017 data sets individually, then jointly. Results of the individual fits are shown in Table 3. The confidence limits were calculated simultaneously for all free model parameters. We find that the RELXILL models produce a similar fit quality as the warm absorber models for the 2000 data set and the black body component models for the 2017 data set.

Assuming that the reflection component causes the soft excess, we obtain a very large spin for the 2017 data set. Due to the large spin and a low reflection fraction, the modeled iron line is heavily broadened and rather inconspicuous in the 2017 data set, while in the 2000 data set the line is more visible due to increased reflection fraction (by a factor of two). We also explored the scenario where a change in the location of the illuminating source to the accretion disk explains the time variable spectral features. For this, we fit the data with the lamp-post scenario (RELXILLLP). In this model, we allow the height ($h$) of the primary radiating source to vary freely. However, we find no significant differences in the heights between the two epochs. The lower limits of the spin values that were produced by either the RELXILL or RELXILLLP models are significantly different for the first epoch.

We also attempted to fit the XMM-2000 and XMM+NuSTAR-2017 data sets with the reflection model affected by a warm absorber (hereafter WA*RELXILL). The 2000 spectrum can be well fit ($\chi^2$/d.o.f. = 134.2/131) with this model similar to the non-WA reflection model, so we do not find any significant improvement in the fits. The lower limit of the spin is, however, affected when including the warm absorber in the fit of XMM-2000 data ($a \geq 0.46$). While the WA*RELXILL can model the soft excess of the 2017 spectrum well, it fails to fit the hard X-ray component ($>30$ keV). This is in accordance with the results by Risaliti et al. (2013), who found for a much higher S/N ratio of NGC 1365 that partial covering absorption models can effectively fit the data up to 10 keV; but they deviate from the data at higher energies.

In addition, we performed a joint fit to the combined 2000 and 2017 data sets with the RELXILL model. A joint-fit consists of linked and unlinked parameters. Linked parameters are values which we assume do not change in human timescales, such as the BH spin, the disk inclination, the ionization parameter and the iron abundance. Since we have not found any significant differences in the neutral hydrogen column density for the two XMM-epochs (see Table 2), we let this also be a linked parameter. The unlinked parameters, such as the power-law photon index, normalization, and the reflection fraction, were allowed to vary independently.

The best fit produces a nearly maximal spin of $a \geq 0.98$ with the disk inclination pegged to the maximum allowed value of 41° (see Table 4). Additionally, the values of the other parameters appear to be similar to the values obtained in Table 3. The joint-fit model of the multi-epoch spectra is shown in Fig. 4. Here, we note that we have also studied cases, where the
inclination angle is fixed to lower values (see Table A.1), such as 22° (Liodakis et al. 2018) and 35° (Hovatta et al. 2009) with a clear impact being to the value of iron abundance, the ionization parameter, and the reflection fraction. As a sanity check, we also fit the data allowing the irradiation profile parameters to vary freely. The model converges at steep power-laws ($\beta_1 = 8.8$ and $\beta_2 = 3.1$ with $R_{\text{in}} = 2.8 R_g$) as is expected if the reflection comes from the inner accretion disk. The increase in the number of free parameters leads to a fit that is slightly better statistically ($\chi^2$/d.o.f. = 669.5/595), but it does not properly reproduce the hard X-ray part of the spectrum. Therefore, we favor the fit where the irradiation profile is kept fixed.

We note that the RELXILL model is able to fit both spectra well by only varying the reflection factor, power-law index, and normalization. On the other hand, as shown in Fig. 1, the X-ray flux has clearly increased in the $0.23-10$ keV range for over 17 years. One possible explanation for the increased X-ray luminosity is the change in the mass accretion rate by a factor of $\sim 2$.

Since the best fit of the combined data set in Table 4 gives an inclination at the upper edge of the allowed range, we have extended our analysis by fitting the RELXILL model to the data that also have a wide range of assumed disk inclinations. The results of these fits to the combined 2000+2017 data set are shown in Appendix A (see Table A.1). By letting the inclination vary freely, it settles on $\theta = 55^\circ \pm 2^\circ$. For this model, the black hole spin is higher than 0.99. The overall fit quality as a function of inclination shows a clear valley around $\sim 50^\circ$. Both low ($\lesssim 20^\circ$) and high ($\gtrsim 60^\circ$) inclination cases produce a poor fit to the iron line.

Finally, we extended the analysis to examine the quality of the fit for a wide range of spin values. The results are displayed in Table B.1. The minimum $\chi^2$ value is found at the very high (positive) black hole spin ($a = 0.992$). Overall, we find a lower fit quality when the spin is set to values $\lesssim 0.9$. In addition, low positive and all negative spin values show a strong tendency toward very large disk inclinations (hitting the upper limit of $80^\circ$), subsolar iron abundances, and low reflection fractions for both epochs. Given the limits to the jet inclination angle derived from the radio observations, and the fact that III Zw 2 is a type 1 AGN with prominent broad emission lines (Marziani et al. 2003), we consider it rather unlikely that the disk inclination would be so high. We discuss this further in the next section.

4. Summary and discussion

We study the X-ray spectrum of III Zw 2 for three different X-ray observations made in 2000, 2011, and 2017. To explore the presence of a soft X-ray component and an Fe Kα line in the data, we first applied phenomenological power-law models. These results have shown a visible soft-excess component in the 2000 (Gonzalez et al. 2018) and 2017 data sets. In addition, a prominent iron line has been observed in the XMM-2000 data (Salvi et al. 2002; Piconcelli et al. 2005; Gonzalez et al. 2018). We study whether the soft excess and the iron line can be fit with a reflection model.

The black hole spin of III Zw 2 was constrained by applying the relativistic reflection model RELXILL. We estimated the BH spin using two different methods: by fitting the data separately and by combining the two observation epochs (2000 and 2017) under the joint-fit approach. In both methods, we set an upper limit of $41^\circ$ for the disk inclination. Fitting the 2000 spectrum alone produces a lower limit for the spin of $a \gtrsim 0.78$, while the 2017 spectrum gives $a \gtrsim 0.98$. Since the BH spin is not expected to change in a time scale of years, a joint-fit is considered as a preferable method to determine the spin of III Zw 2. The joint fit favors a large spin value with a lower limit, $a \gtrsim 0.98$. We note that the quoted lower limits correspond to the statistical uncertainty of the fit, and they do not take any systematic effects into account. While systematics are difficult to assess, we can use the results of Bonson & Gallo (2016) as a guideline. Those authors have studied the ability of the standard fitting procedure to recover the correct model parameters from a large number of simulated Seyfert 1 spectra. Their results indicate that spin can be measured with confidence to an accuracy of about $\pm 0.1$ for high spin cases ($a > 0.8$), especially if the measured spectrum extends up to $70$ keV. Finally, we note that large spin values (0.85 < $a < 0.92$) have been also reported by Gnedin et al. (2012). Their results are based on spectropolarimetric observations combined with the jet kinetic power and assuming a large disk inclination angle of $60^\circ$.

The estimation of the black hole spin by fitting a relativistic reflection model has naturally a number of caveats, which we discuss below.

Table 4. RELXILL joint-fit parameters of the combined XMM-2000 and XMM+NuSTAR 2017 spectra.

| Linked parameters | Unlinked parameters |
|-------------------|---------------------|
| $\theta$ | $a$ | $N_H$ | $\log(\xi)$ | $A_{Fe}$ |
| $41^\circ+10^\circ$ | $\gtrsim 0.98$ | $0.10^{+0.04}_{-0.03}$ | $2.70^{+0.02}_{-0.05}$ | $2.0 \pm 0.6$ |

Notes. $N_H$ is given in units of $10^{22}$ cm$^{-2}$, $\xi$ in units of erg cm s$^{-1}$, $A_{Fe}$ in solar units, and the power law normalization factor with the units of $10^{-5}$ photons keV$^{-1}$ cm$^{-2}$ s$^{-1}$ at 1 keV.

Fig. 4. Joint-fit of the combined 2000 and 2017 data sets with the RELXILL model (blue line). The data-to-model ratio is shown in the lower panel. The model fits the iron line as a heavily broadened and asymmetric feature, indicating emission from very close to the black hole event horizon.
– It is possible that the X-ray spectrum is affected by intervening partially ionized absorbing material. If this is the case, the magnitude and the shape of the reflected component would be different from what is assumed here depending on the amount of absorption and this could affect our results presented above. While we cannot exclude such a warm absorber model, it requires an additional black body component of an unspecified origin in order to fit the data. Therefore, here, we favor the reflection scenario as it is able to fit the data within a single physical scenario without adding phenomenological components.

– Since the black hole spin in our model fits is sensitive to the assumed disk inclination, it is important to have external constraints for it. Throughout this work we assume that the accretion disk is perpendicular to the jet and the jet viewing angle is constant. The alignment of the jet with the angular momentum vector of the disk is the simplest assumption and it has some observational support from the measurements of the X-ray binary system XTE J1550–564 (Steiner & McClintock 2012). Recent general relativistic magneto-hydrodynamic simulations of tilted accretion disks around black holes have shown that the disk and the jet are generally well-aligned (Liska et al. 2018). However, the Bardeen-Petterson effect can align the jet and the disk with the black hole spin axis at small radii (less than a few $R_g$) rapidly compared to the viscous time scale in which the whole disk-jet system aligns with the black hole spin axis (Liska et al. 2019a). This can temporarily leave the outer jet misaligned with respect to the inner accretion disk. It is not clear how large this misalignment can be, but, for example, the simulations performed by Liska et al. (2019b) indicate $\lesssim 15^\circ$ difference even when the disk is originally tilted by $60^\circ$ with respect to the black hole spin axis. Hence, while we cannot exclude the possibility that the inner disk inclination differs from the jet inclination, misalignment of tens of degrees seems unlikely.

– The jet direction may not stay constant over time. While a precessing jet has been suggested for III Zw 2 based on the quasi-periodic variations in its radio flux curves (Li et al. 2010), the measured jet kinematics rule out a large precession angle. Namely, there are three emission features which were ejected into the VLBI jet of III Zw 2 during the past 20 years and which have robust kinematics measurements. All of them are moving in the same direction with the position angles of their motion differing less than $\approx 8^\circ$ (Brunthaler et al. 2000, 2005; Lister et al. 2019)

– We find no prominent Fe Kα line emission in the 2017 spectrum. This behavior seems to be well explained by a heavy broadening of the iron line due to a high spin and a variable reflection fraction, which might be a signature of a change in the disk and/or corona geometry during a flare event or during a post-flare event, leading to decreased illumination in the disk. However, 37 GHz radio observations of III Zw 2 show that the source was in a very low radio state in 2000 and 2017. The epochs are highlighted in Fig. 5.

– We do not discard the possibility of X-ray emission from the jet, which is known to dominate the radio emission from III Zw 2. This emission might have swamped the iron line and contaminated the continuum spectrum in 2017. However, we note that the power law photon indices in 2000 and 2017 model fits are on average close to 1.8, which is similar to what was found in radio-quiet quasars (Piconcelli et al. 2005) associated with the Comptonized hot corona of the disk (Landt et al. 2008). On the contrary, the spectrum in 2011 is highly absorbed with a photon index close to 1.6 that is similar to that of radio-loud quasars (Piconcelli et al. 2005). Thus, we suggest that the 2011 spectrum has an additional X-ray contribution from the jet, which is most likely due to Synchrotron-Self Compton emission. In addition to this, it is interesting to note that the Suzaku observation in 2011 coincides with the rising part of a small radio flare at 37 GHz, while the 2000 and 2017 X-ray observations coincide with very low radio flux states that are indicative of a low jet contribution (see Fig. 5). Thus, here, we suggest that in general a good strategy would be to perform X-ray observations when these types of sources are in their lowest radio state. This may indicate a suitable condition for the detection of the reflection component.

If the observed excesses below 1 keV and at 5–7 keV in the spectrum of III Zw 2 are due to inner disk reflection, our modeling indicates a nearly maximally spinning black hole for this source. This result is the same whether using our initial assumption on the maximum disk inclination (41°) or allowing the disk inclination to vary freely (see Table A.1). While the limit of $a \geq 0.98$ corresponds to statistical uncertainties only and does not include systematic effects, such as the finite thickness of the accretion disk (Taylor & Reynolds 2018), our results do favor a fast-spinning BH in a source that belongs to a group of radio-intermediate quasars, which have been suggested to be relativistically beamed counterparts of radio-quiet quasars (Falcke et al. 1996b). If the jet in III Zw 2 is indeed intrinsically weak, this suggests that spin is not the only parameter driving the vast differences in jet production efficiencies of accreting black holes.

Since the radio emission from the extended jet in III Zw 2 is very weak compared to its beamed core emission (Falcke et al. 1996a; Cooper et al. 2007) and since its optical emission is dominated by the accretion disk (Chen et al. 2012), we can estimate the intrinsic radio-loudness of III Zw 2 by simply scaling the observed radio-loudness by $\delta^{-1}$, where $\delta$ is the relativistic Doppler factor and we have assumed a continuous jet with a spectral index of $\approx -0.5$ (Hovatta et al. 2014). The range of reported radio-loudness in III Zw 2 is 150–200 (Falcke et al. 1996b; Sikora et al. 2007) and the Doppler factor estimates

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6 Liao et al. (2016) even propose that the spectral energy distribution of III Zw 2 can be well-fit by a single-zone, leptonic blazar model during the rapid $\gamma$-ray flare in 2009.
References

Ai, Y. L., Yuan, W., Zhou, H. Y., Wang, T. G., & Zhang, S. H. 2010, ApJ, 727, 31
Blandford, R. D. 1999, in Astrophysical Discs – An EC Summer School, eds. J. A. Sellwood, & J. Goodman, ASP Conf. Ser., 160, 265
Blandford, R. D., & Znajek, R. L. 1977, MNRAS, 179, 433
Bonson, K., & Gallo, L. C. 2016, MNRAS, 458, 1927
Brunthaler, A., Falcke, H., Bower, G. C., et al. 2005, A&A, 435, L49
Brunthaler, A., Falcke, H., Bower, G. C., et al. 2005, A&A, 435, 497
Chen, L., Cao, X., & Bai, J. M. 2012, ApJ, 748, 119
Cooper, N. J., Lister, M. L., & Kochanek, M. D. 2007, ApJS, 171, 376
Dauser, T., Wilms, J., Reynolds, C. S., & Brenneman, L. W. 2010, MNRAS, 409, 1534
Dauser, T., Garcia, J., Wilms, J., et al. 2013, MNRAS, 430, 1694
Dauser, T., Garcia, J., Parker, M. L., Fabian, A. C., & Wilms, J. 2014, MNRAS, 444, L100
Dauser, T., Garcia, J., & Wilms, J. 2016, Astron. Nachr., 337, 362
Done, C., & Nayakshin, S. 2007, MNRAS, 377, L59
Done, C., Gierliński, M., Sobolewska, M., & Schurch, N. 2007, in The Central Engine of Active Galactic Nuclei, eds. L. C. Ho, & J. W. Wang, ASP Conf. Ser., 373, 121
Falcke, H., Patnaik, A. R., & Sherwood, W. 1996a, ApJ, 473, L13
Falcke, H., Sherwood, W., & Patnaik, A. R. 1996b, ApJ, 471, 106
Falcke, H., Bower, G. C., Lohman, A. P., et al. 1999, ApJ, 514, L17
García, J., & Kallman, T. R. 2010, ApJ, 718, 695
García, J., Kallman, T. R., & Mushotzky, R. F. 2011, ApJ, 731, 131
García, J., Dauser, T., Reynolds, C. S., et al. 2013, ApJ, 768, 146
García, J., Dauser, T., Lohfink, A., et al. 2014, ApJ, 782, 76
García, J. A., Fabian, A. C., Kallman, T. R., et al. 2016, MNRAS, 462, 751
Gierliński, M., & Done, C. 2004, MNRAS, 349, L7
Gnedin, Y. N., Afanasiev, V. L., Borisov, N. V., et al. 2012, Astron. Rep., 56, 573
Gonzalez, A. G., Waddell, S. G. H., & Gallo, L. C. 2018, MNRAS, 475, 128
Grier, C. J., Peterson, B. M., Pogge, R. W., et al. 2012, ApJ, 755, 60
Hao, C. N., Xia, X. Y., Mao, S., Wu, H., & Deng, Z. G. 2005, ApJ, 625, 78
Houck, J. C., & Denicola, L. A. 2000, in Astronomical Data Analysis Software and Systems IX, eds. M. Sanset, C. Veillet, & D. Crabtree, ASP Conf. Ser., 216, 591
Hovatta, T., Valtaoja, E., Tornikoski, M., & Lähteenmäki, A. 2009, A&A, 494, 527
Hovatta, T., Aller, M. F., Aller, H. D., et al. 2014, AJ, 147, 143
Inoue, H., Terashima, Y., & Ho, L. C. 2007, ApJ, 662, 860
Jiménez-Bailón, E., Piconcelli, E., Guainazzi, M., et al. 2005, A&A, 435, 499
Kalberla, P. M. W., Burton, W. B., Hartmann, D. et al. 2005, A&A, 440, 775
Khachikian, E. Y., & Weedman, D. W. 1974, ApJ, 192, 581
Landt, H., Padovani, P., Giommi, P., Perri, M., & Cheung, C. C. 2008, ApJ, 687, 87
Laor, A. 2019, Nat. Astron., 3, 374
Li, H. Z., Xie, G. Z., Dai, H., et al. 2010, New Astron., 15, 254
Liao, N.-H., Yin, Y.-L., Fan, X.-L., et al. 2016, ApJ, 226, 17
Liodakis, I., Hovatta, T., Happenkothen, D., et al. 2018, ApJ, 866, 137
Liska, M., Hesp, C., Tchekhovskoy, A., et al. 2018, MNRAS, 474, L81
Liska, M., Tchekhovskoy, A., Ingram, A., & van der Klis, M. 2019a, MNRAS, 487, 550
Liska, M., Hesp, C., Tchekhovskoy, A., et al. 2019b, MNRAS, submitted [arXiv:1901.05979]
Lister, M. L., Aller, M. F., Aller, H. D., et al. 2018, ApJ, 234, 12
Lister, M. L., Homan, D. C., Hovatta, T., et al. 2019, ApJ, 874, 43
Marziani, P., Sulentic, J. W., Zamanov, R., et al. 2003, ApJS, 145, 199
McKinney, J. C., Tchekhovskoy, A., & Blandford, R. D. 2012, MNRAS, 423, 2083
Narayan, R., Igumenschev, I. V., & Abramowicz, M. A. 2003, PASJ, 55, L69
Piconcelli, E., Jimenez-Bailón, E., Guainazzi, M., et al. 2005, A&A, 432, 15
Porquet, D., Reeves, J. N., O’Brien, P., & Brinkmann, W. 2004, A&A, 422, 85
Pushkarev, A. B., Hovatta, T., Kovalev, Y. Y., et al. 2012, A&A, 545, A113
Reynolds, C. S. 2014, Space Sci. Rev., 183, 277
Reynolds, C. S. 2019, Nat. Astron., 3, 41
Reynolds, C. S., & Fabian, A. C. 2008, ApJ, 675, 1048
Risaliti, G., Harrison, F. A., Madsen, K. K., et al. 2013, Nature, 494, 449
Salvi, N. J., Page, M. J., Stevens, J. A., et al. 2002, MNRAS, 335, 177
Schmidt, M., & Green, R. F. 1983, ApJ, 266, 352
Sikora, M., & Begelman, M. C. 2013, ApJ, 764, L24
Sikora, M., Stawarz, L., & Lasota, J.-P. 2007, ApJ, 658, 815
Steiner, J. F., & McClintock, J. E. 2012, ApJ, 745, 136
Taylor, C., & Reynolds, C. S. 2018, ApJ, 855, 120
Tchekhovskoy, A., Narayan, R., & McKinney, J. C. 2010, ApJ, 711, 50
Tchekhovskoy, A., Narayan, R., & McKinney, J. C. 2011, MNRAS, 418, L79
Teräsranta, H., Tornikoski, M., Muñen, A., et al. 1998, A&AS, 132, 305
Vestergaard, M., & Peterson, B. M. 2006, ApJ, 641, 689
Volonteri, M. 2010, in Accretion and Ejection in AGN: A Global View, eds. L. Maraschi, G. Ghisellini, R. Della Ceca, & F. Tavecchio, ASP Conf. Ser., 427, 3
Volonteri, M., Madau, P., Quataert, E., & Rees, M. J. 2005, ApJ, 620, 69
Walton, D. J., Nardini, E., Fabian, A. C., Gallo, L. C., & Reis, R. C. 2013, MNRAS, 428, 2901
Wilson, A. S., & Colbert, E. J. M. 1995, ApJ, 438, 62
Yuan, W., Liu, B. F., Zhou, H., & Wang, T. G. 2010, ApJ, 723, 508
Zamfirescu, M., Clausen-Brown, E., Savolainen, T., & Tchekhovskoy, A. 2014, Nature, 510, 126
Zhong, X., & Wang, J. 2013, ApJ, 773, 23
Appendix A: Different disk inclination values

Below we show the best-fit parameters for RELXILL models that have different fixed disk inclination values as well as for the freely varying, nonconstrained inclination case. The joint-fit with RELXILL is given to the combined 2000 and 2017 spectra. We use the same fixed values for the irradiation profile and disk radius parameters as described in Sect. 3.2. The joint-fits of the iron line region are displayed in Fig. A.1. The figure shows the 3–9 keV part of the spectrum.

At lower angles, the models of the iron line are skewed toward the left side whereas at higher angles the fits display a linear tendency with a change in the slope. The models around the line resemble a broadened and asymmetric feature when the disk inclination lies, for instance, between 40 and 55°.

Table A.1. RELXILL joint-fit results for different disk inclinations.

| $\theta$ (°) | $a$ | $\Gamma_{2000}$ | $\Gamma_{2017}$ | log($\xi$) (erg cm s$^{-1}$) | $A_{\text{Fe}}$ (solar) | $R_{2000}$ | $R_{2017}$ | $\chi^2$/d.o.f. |
|--------------|-----|-----------------|-----------------|-----------------------------|------------------------|----------|----------|----------------|
| 5°           | ≥0.976 | 1.78±0.02       | 1.87±0.02       | 2.73±0.04                   | 2.71±0.50              | 1.04±0.18 | 0.55±0.07 | 777/599 (1.30) |
| 10°          | ≥0.978 | 1.76±0.02       | 1.87±0.02       | 2.73±0.04                   | 2.67±0.50              | 1.04±0.18 | 0.56±0.06 | 772/599 (1.29) |
| 22°          | ≥0.983 | 1.78±0.02       | 1.87±0.02       | 2.73±0.05                   | 2.47±0.51              | 1.07±0.18 | 0.56±0.06 | 746/599 (1.25) |
| 35°          | ≥0.986 | 1.77±0.03       | 1.87±0.02       | 2.71±0.02                   | 2.18±0.52              | 0.99±0.17 | 0.52±0.06 | 710/599 (1.19) |
| 40°          | ≥0.988 | 1.77±0.03       | 1.87±0.01       | 2.70±0.04                   | 2.05±0.54              | 0.93±0.15 | 0.49±0.05 | 698/599 (1.17) |
| 50°          | ≥0.992 | 1.76±0.02       | 1.86±0.01       | 2.70±0.02                   | 1.56±0.54              | 0.83±0.15 | 0.43±0.05 | 691/599 (1.15) |
| 60°          | ≥0.993 | 1.73±0.02       | 1.84±0.01       | 2.70±0.07                   | 1.19±0.65              | 0.56±0.09 | 0.31±0.03 | 693/599 (1.17) |
| 70°          | ≥0.993 | 1.85±0.02       | 1.92±0.02       | 1.30±0.08                   | 0.72±0.23              | 0.48±0.07 | 0.31±0.03 | 708/599 (1.18) |
| 80°          | ≤0.298 | 1.82±0.01       | 1.89±0.01       | 1.11±0.20                   | 0.64±0.26              | 0.29±0.01 | 0.18±0.03 | 729/599 (1.22) |
| 55° ± 2°     | ≥0.992 | 1.74±0.02       | 1.85±0.01       | 2.70±0.02                   | 1.57±0.51              | 0.64±0.15 | 0.35±0.05 | 685/598 (1.15) |

Notes. The last row shows the results for a freely varying disk inclination. ∗This model does not fit the iron line well. The plots exhibiting this effect are displayed in Fig. A.1.
Appendix B: Different spin values

Below we show the RELXILL fits of the combined 2000 and 2017 data sets. The best-fit parameters are displayed for different fixed spin values. The disk inclination and the other parameters vary freely.

Table B.1. RELXILL joint-fit results for different spin values.

| $a$  | $\theta$ | log($\xi$) | $A_{Fe}$ | $R_{2000}$  | $R_{2017}$  | $\chi^2$/d.o.f. |
|------|----------|-------------|----------|-------------|-------------|-----------------|
| 0.992| $55^\circ \pm 3^\circ$ | 2.70$^{+0.02}_{-0.07}$ | 1.35$^{+0.69}_{-0.37}$ | 0.64$^{+0.13}_{-0.11}$ | 0.35$^{+0.04}_{-0.03}$ | 688.3/599 (1.15) |
| 0.900| $46^\circ \pm 4^\circ$ | 2.70$^{+0.01}_{-0.05}$ | 1.29$^{+0.80}_{-0.31}$ | 0.59$^{+0.12}_{-0.08}$ | 0.30$^{+0.04}_{-0.03}$ | 726.6/599 (1.21) |
| 0.800| $62^\circ \pm 4^\circ$ | 1.30$^{+0.08}_{-0.15}$ | 0.66$^{+0.22}_{-0.10}$ | 0.43$^{+0.08}_{-0.07}$ | 0.26$^{+0.03}_{-0.04}$ | 735.6/599 (1.23) |
| 0.700| $62^\circ \pm 7^\circ$ | 1.30$^{+0.05}_{-0.23}$ | 0.59$^{+0.23}_{-0.09}$ | 0.42$^{+0.06}_{-0.10}$ | 0.25$^{+0.03}_{-0.05}$ | 736.2/599 (1.23) |
| 0.500| $66^\circ \pm 14^\circ$ | 1.29$^{+0.05}_{-0.55}$ | 0.66$^{+0.24}_{-0.10}$ | 0.39$^{+0.07}_{-0.11}$ | 0.23$^{+0.03}_{-0.05}$ | 733.9/599 (1.22) |
| 0.300| $78^\circ \pm 8^\circ$ | 1.07$^{+0.25}_{-0.27}$ | 0.63$^{+0.26}_{-0.13}$ | 0.32$^{+0.10}_{-0.07}$ | 0.20$^{+0.03}_{-0.02}$ | 730.9/599 (1.22) |
| 0.100| $78^\circ \pm 2^\circ$ | 1.09$^{+0.23}_{-0.08}$ | 0.64$^{+0.25}_{-0.14}$ | 0.32$^{+0.09}_{-0.06}$ | 0.20$^{+0.03}_{-0.02}$ | 728.6/599 (1.22) |
| 0   | $78^\circ \pm 2^\circ$ | 1.11$^{+0.21}_{-0.09}$ | 0.64$^{+0.25}_{-0.14}$ | 0.32$^{+0.08}_{-0.07}$ | 0.20$^{+0.03}_{-0.02}$ | 728.7/599 (1.21) |
| $-0.100$ | $78^\circ \pm 2^\circ$ | 1.12$^{+0.19}_{-0.09}$ | 0.64$^{+0.25}_{-0.14}$ | 0.32$^{+0.08}_{-0.07}$ | 0.20$^{+0.03}_{-0.02}$ | 727.3/599 (1.21) |
| $-0.300$ | $78^\circ \pm 1^\circ$ | 1.15$^{+0.17}_{-0.11}$ | 0.65$^{+0.25}_{-0.15}$ | 0.32$^{+0.07}_{-0.06}$ | 0.20$^{+0.04}_{-0.03}$ | 726.7/599 (1.21) |
| $-0.500$ | $78^\circ \pm 1^\circ$ | 1.18$^{+0.15}_{-0.12}$ | 0.65$^{+0.25}_{-0.15}$ | 0.32$^{+0.08}_{-0.05}$ | 0.20$^{+0.04}_{-0.02}$ | 727.8/599 (1.21) |
| $-0.700$ | $77^\circ \pm 2^\circ$ | 1.22$^{+0.12}_{-0.14}$ | 0.66$^{+0.24}_{-0.16}$ | 0.32$^{+0.08}_{-0.05}$ | 0.20$^{+0.04}_{-0.02}$ | 727.6/599 (1.21) |
| $-0.800$ | $77^\circ \pm 2^\circ$ | 1.23$^{+0.12}_{-0.15}$ | 0.66$^{+0.24}_{-0.16}$ | 0.32$^{+0.08}_{-0.05}$ | 0.20$^{+0.02}_{-0.01}$ | 727.2/599 (1.21) |
| $-0.900$ | $77^\circ \pm 2^\circ$ | 1.25$^{+0.10}_{-0.16}$ | 0.66$^{+0.24}_{-0.16}$ | 0.32$^{+0.08}_{-0.05}$ | 0.20$^{+0.02}_{-0.01}$ | 726.9/599 (1.21) |
| $-0.992$ | $77^\circ \pm 2^\circ$ | 1.26$^{+0.09}_{-0.16}$ | 0.66$^{+0.24}_{-0.16}$ | 0.32$^{+0.08}_{-0.05}$ | 0.20$^{+0.02}_{-0.01}$ | 726/599 (1.22) |