A review of machine learning methods to predict the solubility of overexpressed recombinant proteins in *Escherichia coli*

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**Abstract**

**Background:** Over the last 20 years in biotechnology, the production of recombinant proteins has been a crucial bioprocess in both biopharmaceutical and research arena in terms of human health, scientific impact and economic volume. Although logical strategies of genetic engineering have been established, protein overexpression is still an art. In particular, heterologous expression is often hindered by low level of production and frequent fail due to opaque reasons. The problem is accentuated because there is no generic solution available to enhance heterologous overexpression. For a given protein, the extent of its solubility can indicate the quality of its function. Over 30% of synthesized proteins are not soluble. In certain experimental circumstances, including temperature, expression host, etc., protein solubility is a feature eventually defined by its sequence. Until now, numerous methods based on machine learning are proposed to predict the solubility of protein merely from its amino acid sequence. In spite of the 20 years of research on the matter, no comprehensive review is available on the published methods.

**Results:** This paper presents an extensive review of the existing models to predict protein solubility in *Escherichia coli* recombinant protein overexpression system. The models are investigated and compared regarding the datasets used, features, feature selection methods, machine learning techniques and accuracy of prediction. A discussion on the models is provided at the end.

**Conclusions:** This study aims to investigate extensively the machine learning based methods to predict recombinant protein solubility, so as to offer a general as well as a detailed understanding for researches in the field. Some of the models present acceptable prediction performances and convenient user interfaces. These models can be considered as valuable tools to predict recombinant protein overexpression results before performing real laboratory experiments, thus saving labour, time and cost.

**Keywords:** Protein solubility, Protein solubility prediction, In silico prediction, Recombinant protein expression, *Escherichia coli*, Machine learning, Bioinformatics, Computational biology

**Introduction**

In biotechnology, production of recombinant proteins is a crucial process in both biopharmaceutical industries and scientific research. So far, *Escherichia coli* (*E. coli*), a bacterium that requires simple conditions to grow is still the favoured host for cloning and overexpressing most proteins which are non-glycosylated and do not have many cysteine residues [1].

Even though logical strategies of genetic engineering are well established, such as strong promoters and codon optimization, protein overexpression is often still an art. In particular, heterologous expression is often afflicted with low levels of production and insoluble recombinant proteins forming inclusion bodies (protein aggregations). Yet, there is no generic solution available to enhance heterologous overexpression. The use of fusion proteins can sometimes be more successful at the expense of decreased total yield as a result of the fusion partner production. Features that differentiate between proteins in the negative (non-expressed) and positive (expressed) classes might indicate sequence characteristics...
| #  | Paper | Dataset(s) | Feature selection method(s) | Modeling technique(s) | Web server |
|----|-------|------------|-----------------------------|-----------------------|------------|
| 1  | [7]   | Bacterial protein sequences with ‘soluble’ and ‘insoluble’ in NCBI are selected randomly. | Wrapper: SVM | Support vector machine | -          |
|    |       | Size: 5692 |                             |                       |            |
|    |       | Soluble: 2448 |                           |                       |            |
|    |       | Insoluble: 3244 |                         |                       |            |
| 2  | [10]  | HGPD       | Filter: Student’s t-test   | Two techniques:       | ESPRESSO:  |
|    |       | E. coli    |                             |                       |            |
|    |       | Size: 5100 |                             |                       |            |
|    |       | Soluble: 1774 |                          |                       |            |
|    |       | Insoluble: 3326 |                        |                       |            |
|    |       | Wheat germ |                             |                       |            |
|    |       | Size: 2939 |                             |                       |            |
|    |       | Soluble: 1941 |                          |                       |            |
|    |       | Insoluble: 998 |                         |                       |            |
| 3  | [5]   | eSol       | Two methods:                | Random forest         | ProS:      |
|    |       | Size: 1918 | 1. Filter: Student’s t-test |                       |            |
|    |       | Soluble: 886 |                             |                       |            |
|    |       | Insoluble: 1032 |                        |                       |            |
| 4  | [8]   | Four datasets: | -                           | Two methods:         | SCM:       |
|    |       | Sd957      |                             |                       |            |
|    |       | Dataset Chan et al. [18] (Table 1, row 11) |             |                       |            |
|    |       | Solpro     |                             |                       |            |
|    |       | PROSO II   |                             |                       |            |
| 5  | [4]   | eSol       | -                           | Four techniques:     | -          |
|    |       | Size: 1600 |                             |                       |            |
|    |       |             | 1. Support vector machine   |                       |            |
|    |       |             | 2. Random forest            |                       |            |
|    |       |             | 3. Conditional inference trees |                     |            |
|    |       |             | 4. Rule ensemble             |                       |            |
| 6  | [6]   | PROSO II   | Wrapper                     | A two-layer model:   | PROSOII:   |
|    |       |             |                             |                       |            |
|    |       |             | 1. Layer 1: Parzen window + logistic regression |            | mips.helmholtz-muenchen.de/prosoll |
|    |       |             | 2. Layer 2: Logistic regression |                    |            |
| No. | Reference | Methodology | Classification | Size (Training) | Soluble (Training) | Insoluble (Training) | Species | Size (Test) | Soluble (Test) | Insoluble (Test) | Non-expressed (Test) |
|-----|-----------|-------------|----------------|----------------|-------------------|---------------------|---------|-------------|----------------|------------------|---------------------|
| 7   | [22]      | eSol        | Decision tree  | -              | 1625              | 843                 | -       | 782         | -              | -                | -                   |
| 8   | [23]      | eSol        | Wrapper: SVM   | Support vector machine | 2159             | 1081                | 1078                | -       | -           | -              | -                | -                   |
| 9   | [3]       | HGPD        | Filer: Student’s t-test | Random forest | -                   | 2796                | 5027                | -       | 7823        | 2739            | 1216              | E. coli, Wheat germ |
| 10  | [24]      | SOLP        | Seven methods: | Support vector machine | -                   | 2716                | 5027                | -       | 3955        | 2739            | 1216              | -                   |
|     |           |             | 1. Filter: Information gain | -           | 231               | 236                 | -       | 259         | -              | -                | 121 genes from different species were expressed in 6 different vectors. |

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http://www.biomedcentral.com/1471-2105/15/134
| No. | Study | Methodology | Model Details | Dataset Size | Soluble | Insoluble |
|-----|--------|-------------|---------------|--------------|---------|-----------|
| 12  | [20]   | A database collected through literature search. | N/A | Logistic regression | http://www.biotech.ou.edu/ |
|     |        | Size: 212 | Soluble: 52 | Insoluble: 160 |
| 13  | [17]   | Solpro | Wrapper | A two-layer model: | SOLpro: scratch.proteomics.ics.uci.edu |
|     |        |        |             | Layer 1: 20 Support vector machines | |
|     |        |        |             | Layer 2: One support vector machine | |
| 14  | [25]   | eSol | Using histogram | Support vector machine | - |
| 15  | [19]   | PROSO | Two methods: | A two-layer model: | PROSO: http://mips.helmholtz-muenchen.de/proso/ |
|     |        |        | 1. Wrapper | Layer 1: Support vector machine | |
|     |        |        | 2. Filter: Symmetrical uncertainty | Layer 2: Naive Bayes | |
| 16  | [26]   | Idicula-Thomas 2006 | N/A | Support vector machine | - |
| 17  | [27]   | Idicula-Thomas 2006 | Filter: Unbalanced correlation score | Support vector machine | - |
| 18  | [28]   | Idicula-Thomas 2005 | Filter: Mann–Whitney test | Discriminant analysis | - |
|     |        |        |             | (A heuristic approach of computing solubility index (SI)) | |
| 19  | [29]   | Genes of C. elegans with one expression vector and one Escherichia coli strain. | Filter: Linear correlation coefficient (LCC) | - | - |
|     |        | Size: 4854 | Soluble: 1536 | Insoluble: 3318 |
| 20  | [30]   | TargetDB | Wrapper: Random forest | Decision tree | - |
|     |        | Size: 27,000 | Soluble: 1536 | Insoluble: 3318 |
| 21  | [14]   | SPINE | Wrapper | Decision tree | - |
|     |        | Size: 562 | Soluble: 213 | Insoluble: 143 |
| 22  | [31]   | SPINE | Embedded: Decision tree | Decision tree | - |
|     |        | Size: 356 | Soluble: 213 | Insoluble: 143 |
| 23  | [18]   | Some genes of E. coli were expressed. | N/A | Regression | - |
|     |        | Size: 100 | Soluble: 213 | Insoluble: 143 |
| 24  | [9]    | Some genes of E. coli were expressed. | N/A | Regression | - |
|     |        | Size: 81 | Soluble: 1536 | Insoluble: 3318 |
that could be modified in optimization, corresponding to
what was attained with codon optimization, where se-
quencies of gene are modified to become compatible with
the translational apparatus [2]. As the host expresses the
proteins, one cause of non-expression is the harmful in-
teraction with the metabolism of the host [3].

For a given protein, the extent of its solubility can in-
dicate the quality of its function. In general, over 30% of
recombinant proteins are not soluble [4]. About 33 to 35
percent of all expressed non-membrane proteins are in-
soluble and about 25 to 57 percent of soluble proteins
are prone to aggregate at higher concentrations [5]. For
a determined experimental condition (i.e. temperature,
expression host, etc.), the solubility of a protein is deter-
mined by its sequence [6].

The trial-and-error procedure of protein overexpres-
sion can be avoided by identifying the promising pro-
tiens to improve the experimental success rate [7].
There are two types of approach for predicting solubility
of protein: sequence-based and structure-based. In the
structure-based technique, the free energy difference
between aggregation and solution phases is computed.
This method demands experimentally obtained high reso-
lutions 3D structures which are hard to acquire for
aggregation-prone proteins. Hence, the sequence-based
 technique is a feasible and widely used method. Generally,
the computational sequence-based prediction methods in-
vestigate the protein overexpression in E. coli at the nor-
mal growth temperature of 37°C [8].

The correlation of amino acid sequence and the tendency
to form inclusion body was shown for the first time by Wil-
kinson and Harrison [9]. Later, numerous methods based
on machine learning were proposed to predict the solubil-
ity of proteins merely from amino acid sequences [10].

Protein solubility prediction can be considered a bin-
ary classification task where a classifier should discrim-
nate between soluble proteins (positive samples) and
insoluble proteins (negative samples). There are several
classification methods (learning algorithm) namely, deci-
sion tree (DT) (e.g. C4.5 [11]), k-nearest-neighbour (KNN)
[12], neural network (NN) [13,14], support vector ma-
chine (SVM) [15], etc.

| # | Paper | Accuracy | Area under curve | F-score | Gain | Mathew correlation coefficient | Precision | Recall | Sensitivity | Specificity |
|---|-------|----------|------------------|---------|------|-------------------------------|-----------|--------|-------------|-------------|
| 1 | [7]   | 0.88     | -                | -       | -    | 0.76                          | -         | -      | -           | -           |
| 2*| [10]  | 0.68     | 0.78             | 0.67     | 0.42 | 0.56                          | 0.85      | -      | -           | -           |
|   |       | 0.75     | 0.75             | 0.82     | 0.42 | 0.79                          | 0.86      | -      | -           | -           |
| 3 | [5]   | 0.84     | 0.91             | -       | -    | 0.67                          | -         | -      | 0.82        | 0.85        |
| 4 | [8]   | 0.84     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 5 | [15]  | 0.90     | -                | -       | -    | 0.80                          | 0.80      | -      | -           | -           |
| 6 | [6]   | 0.75     | -                | 1.69     | 0.39 | 0.65                          | 0.76       | 0.73   | -           | -           |
| 7 | [22]  | 0.75     | 0.81             | -       | -    | -                            | -         | -      | -           | -           |
| 8 | [23]  | -        | -                | -       | -    | -                            | -         | -      | -           | -           |
| 9*| [3]   | 0.71     | -                | -       | -    | 0.47                          | 0.67       | -      | -           | -           |
|   |       | 0.71     | -                | -       | -    | 0.85                          | 0.74       | -      | -           | -           |
| 10| [24]  | -        | -                | -       | -    | -                            | -         | -      | -           | -           |
| 11| [1]   | 0.83     | 0.89             | 0.75     | -    | 0.73                          | 0.78       | -      | -           | -           |
| 12| [20]  | 0.94     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 13| [17]  | 0.74     | 0.74             | -       | 1.49 | 0.49                          | 0.74       | -      | -           | -           |
| 14| [25]  | 0.80     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 15| [19]  | 0.72     | 0.78             | -       | 1.43 | 0.43                          | 0.72       | -      | -           | -           |
| 16| [26]  | 0.79     | 0.76             | -       | -    | -                            | -         | -      | 0.68        | 0.85        |
| 17| [27]  | 0.74     | -                | -       | -    | -                            | -         | -      | 0.57        | 0.81        |
| 18| [28]  | 0.72     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 19| [29]  | -        | -                | -       | -    | -                            | -         | -      | -           | -           |
| 20| [30]  | 0.76     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 21| [16]  | 0.63     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 22| [31]  | 0.65     | -                | -       | -    | -                            | -         | -      | -           | -           |
| 23| [18]  | -        | -                | -       | -    | -                            | -         | -      | -           | -           |
| 24| [9]   | 0.88     | -                | -       | -    | -                            | -         | -      | -           | -           |

a. *Results for E. coli and wheat germ are shown respectively.
| #  | Paper | Features |
|----|-------|----------|
| 1  | [7]   | 1. 2-level triangle CGR  
2. Entropy of ‘2-level triangle CGR’  
3. Dipeptide composition based on a different mode of pseudo amino acid composition (PseAAC)  
4. Entropy of ‘dipeptide composition’ |
| 2  | [10]  | Same as row 9 (Reference [3]) |
| 3  | [5]   | 1. Counts of aromatic amino acids  
2. Counts of buried amino acids  
3. Counts of hydrogen bonds  
4. Counts of leucine amino acid  
5. Counts of arginine amino acid  
6. Negative charge  
7. Surface composition of amino acids in intracellular proteins of Mesophiles (percent)  
8. Beta-strand indices for beta-proteins  
9. Flexibility parameter for two rigid neighbours  
10. Net charge  
11. Counts of nitrogen atoms  
12. Long range non-bonded energy per atom  
13. Isometric point (pI)  
14. Free energies of transfer of AcWi-X-LL peptides from bilayer interface to water  
15. Ratio of negative charge amino acids  
16. Ratio of net charge of protein  
17. Dependence of partition coefficient on ionic strength |
| 4  | [8]   | Dipeptide composition (400 features) |
| 5  | [4]   | 1. Reduced features (39 features produced by pepstats):  
a. Molecular weight, number of residues, average residue weight, charge and isoelectric point  
b. For each type of amino acid: number, molar percent and DayhoffStat  
c. For each physicochemical class of amino acid: number, molar percent, molar extinction coefficient (A280) and extinction coefficient at 1 mg/ml (A280)  
2. Dimers (2400 features):  
a. Dimers amino acid frequencies which are computed considering gaps of 1–5 amino acid  
3. Complete set  
a. Reduced features + Dimers |
| 6  | [6]   | 1. Amino acid frequencies (18 features): R, N, D, C, Q, E, G, H, I, K, M, F, P, S, T, W, Y, V  
2. Dipeptide frequencies (13 features): AK, CV, EG, GN, GH, HE, IH, IW, MR, MQ, PR, TS, WD |
| 7  | [22]  | 1. Monomer, dimer and trimmers using 7 different alphabets (18 features)  
2. Sequence-computed features:  
a. Molecular weight  
b. Sequence length  
c. Isoelectric point  
d. GRAVY index  
3. Features used in Niwa et al. work [25]  
4. Combination of all the above features 1–3. |
| 8  | [23] | 1. Coil  
|    |      | 2. Disorder  
|    |      | 3. Hydrophobicity  
|    |      | 4. Hydrophilicity  
|    |      | 5. β-turn  
|    |      | 6. α-helix  |
| 9  | [3]  | 1. Nucleotide sequence information:  
|    |      | a. 1-mer  
|    |      | b. Frequencies of 64 codons (3-mer)  
|    |      | c. GC-contents  
|    |      | 2. Amino acid sequence information:  
|    |      | a. Polypeptide length  
|    |      | b. Frequencies of 20 single amino acids (1-mer)  
|    |      | c. Frequencies of 8 chemical property groups  
|    |      | d. Frequencies of 5 physical property groups  
|    |      | e. Repeat of amino acids  
|    |      | f. Repeat of 8 chemical property groups  
|    |      | g. Repeat of 5 physical property groups  
|    |      | 3. Amino acid structural information:  
|    |      | a. Frequencies of single amino acids in surface area  
|    |      | b. Frequencies of 8 chemical property groups in surface area  
|    |      | c. Frequencies of 5 physical property groups in surface area  
|    |      | d. Number of transmembrane regions  
|    |      | e. Disordered regions:  
|    |      | i. Number of occurrence  
|    |      | ii. Length  
|    |      | iii. Proportion  
|    |      | f. Secondary structures:  
|    |      | i. α-helix  
|    |      | ii. Beta-sheet  
|    |      | iii. Others  |
| 10 | [24] | 1497 features computed by Protein Feature Server (PROFEAT) [32]:  
|    |      | 1. Group 1:  
|    |      | a. Amino acid composition  
|    |      | b. Dipeptide composition  
|    |      | 2. Group 2: Autocorrelation  
|    |      | a. Normalized Moreau-Broto autocorrelation  
|    |      | 3. Group 3: Autocorrelation 2  
|    |      | a. Moran autocorrelation  
|    |      | 4. Group 4: Autocorrelation 3  
|    |      | a. Geary autocorrelation  
|    |      | 5. Group 5:  
|    |      | a. Composition  
|    |      | b. Transition  
|    |      | c. Distribution  |
| Group | Features                                                                                           |
|-------|----------------------------------------------------------------------------------------------------|
| 6.    | Sequence order 1                                                                                  |
|       | a. Sequence-order-coupling number                                                                 |
|       | b. Quasi-sequence-order descriptors                                                                |
| 7.    | Sequence order 2                                                                                   |
|       | a. Pseudo amino acid descriptors                                                                  |
| 11    |                                                                                                   |
| 1.    | Nucleotide information                                                                            |
|       | a. 1-mer                                                                                           |
|       | b. 2-mer                                                                                           |
|       | c. 3-mer                                                                                           |
|       | d. Sequence length                                                                                |
|       | e. GC content                                                                                     |
| 2.    | Amino Acid information                                                                            |
|       | a. Features of Wilkinson and Harrison [9]                                                          |
|       | b. Features of Idicula-Thomas et al. [27]                                                           |
|       | c. Isoelectric point                                                                               |
|       | d. Peptide statistics                                                                              |
| 3.    | Codon Adaptation Index                                                                            |
| 4.    | PTMs                                                                                               |
| 12    |                                                                                                   |
| 1.    | Molecular weight                                                                                  |
| 2.    | Cysteine fraction                                                                                  |
| 3.    | Hydrophobicity-related parameters                                                                  |
|       | a. Fraction of total number of hydrophobic amino acids                                             |
|       | b. Fraction of largest number of contiguous hydrophobic/hydrophilic amino acids                    |
| 4.    | Aliphatic index                                                                                    |
| 5.    | Secondary structure-related properties                                                              |
|       | a. Proline fraction                                                                                |
|       | b. Alpha-helix propensity                                                                          |
|       | c. Beta-sheet Propensity                                                                           |
|       | d. Turn-forming residue fraction                                                                   |
|       | e. Alpha-helix propensity/b-sheet propensity                                                        |
| 6.    | Protein-solvent interaction related parameters                                                     |
|       | a. Hydrophilicity index                                                                            |
|       | b. pl                                                                                             |
|       | c. Approximate charge average                                                                      |
| 7.    | Fractions of: Alanine, Arginine, Asparagine, Aspartate, Glutamate, Glutamine, Glycine, Histidine, |
|       | Isoleucine, Leucine, Lysine, Methionine, Phenylalanine, Serine, Threonine, Tyrosine, Tryptophan     |
|       | and Valine                                                                                         |
| 13    |                                                                                                   |
| 1.    | Frequencies of amino acid monomers, dimers and trimmers using 7 different alphabets:              |
|       | a. Monomer frequencies                                                                             |
|       | i. Natural-20M                                                                                     |
|       | ii. ClustEM-17M                                                                                     |
|       | iii. ClustEM-14M                                                                                    |
|       | iv. PhysChem-7M                                                                                     |
|       | v. BlosumSM-8M                                                                                      |
|       | vi. ConfSimi-7M                                                                                      |
|       | vii. Hydropho-5M                                                                                    |

Table 3 Features used to predict protein solubility (Continued)
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| 14 | [25] | 1. Molecular weight |
|----|------|-------------------|
| 2. Isometric point (pI) |
| 3. Ratios of each amino acid content |

| 15 | [19] | 4. For mono-domain proteins: |
|----|------|-------------------------------|
| a. Word size 1: |
| S, I, M, F, DE, A, C, G, R |
| b. Word size 2: |
| R + R, R + C, R + E, R + T, N + Q, N + H, N + L, C + S, Q + A, Q + G, Q + I, E + A, E + G, E + K, E + P, E + V, G + P, H + M, L + Y, K + G, K + K, M + G, S + S, T + I, Y + C, Y + I |
| c. Word size 3: |
| ST + ST + ST, ST + ST + N, ST + DQE + AH, ST + C + ST, G + M + R, G + K + G, G + P + G, G + P + N, M + AH + AH, M + C + Y, DQE + G + R, DQE + R + DQE, DQE + M + ST, DQE + Y + N, DQE + AH + IV, K + R + IV, K + K + ST, P + DQE + DQE, P + DQE + C, IV + G + IV, L + IV + DQE, N + FW + DQE, N + C + P, AH + ST + ST, AH + K + L, C + FW + Y, C + K + C |

| 5. For multi-domain proteins: |
| a. Word size 1: |
| R, D, C, E, G, L, K, M, S, W |
| b. Word size 2: |
| A + Y, A + V, R + N, R + E, R + S, R + Y, N + A, D + M, C + T, Q + A, Q + E, E + D, E + G, E + T, G + I, G + F, G + S, H + C, H + M, H + P, L + G, L + S, K + D, K + G, K + L, K + F, P + L, T + L, T + Y, V + R |
### Table 3 Features used to predict protein solubility (Continued)

| Features                                                                 |
|--------------------------------------------------------------------------|
| c. Word size 3:                                                          |
| ST + ST + ST, ST + P + DQE, ST + IV + K, R + DQE + FW, R + DQE + IV, R + IV + FW, |
| FW + DQE + FW, M + ST + DQE, M + G + AH, M + FW + DQE, DQE + ST + ST, |
| DQE + ST + G, DQE + G + K, DQE + IV + R, DQE + IV + L, P + G + ST, IV + ST + P, |
| L + K + FW, AH + ST + IV, AH + G + IV, AH + AH + M                        |
| 16 [26]                                                                  |
| 1. Aliphatic index                                                       |
| 2. Frequency of occurrence of residues Cysteine (Cys), Glutamic acid (Glu), Asparagine (Asn) and Tyrosine (Tyr) |
| 3. Reduced class of conformational similarity [CMQLEKRA]                 |
| 4. Reduced classes of hydrophobicity [CFLMW] and [NQSTY]                 |
| 5. Reduced classes of BLOSUM50 substitution matrix [CILMV]                |
| 6. The 18 dipeptide composition: [VC], [AE], [VE], [WF], [YF], [AG], [FG], [WG], [HH], [MI], [HK], [KN], [KP], [ER], [YS], [RV], [KY], [TY] |
| 17 [27]                                                                  |
| 1. Physicochemical properties (6 features):                              |
| a. Length of protein                                                     |
| b. Hydropathy index (GRAVY)                                              |
| c. Aliphatic index                                                       |
| d. Instability index                                                     |
| e. Instability index of N-terminus                                       |
| f. Net charge                                                            |
| 2. Mono-peptide frequencies (20 features)                                |
| 3. Dipeptide frequencies (400 features)                                  |
| 4. Reduced alphabet set (20 features)                                    |
| 18 [28]                                                                  |
| 1. Aliphatic index (AI)                                                  |
| 2. Instability index of the N terminus                                   |
| 3. Frequency of occurrence of Asn, Thr, and Tyr                         |
| 4. Tri-peptide score                                                     |
| 19 [29]                                                                  |
| 1. Signal peptide                                                       |
| 2. GRAVY                                                                 |
| 3. Transmembrane helices                                                |
| 4. Number of Cysteines                                                  |
| 5. Anchor peptide                                                       |
| 6. Prokaryotic membrane lipoprotein lipid attachment site               |
| 7. PDB identity                                                          |
| 20 [30]                                                                  |
| 1. General sequence composition                                          |
| 2. Clusters of orthologous groups (COG) assignment                       |
| 3. Length of hydrophobic stretches                                      |
| 4. Number of low-complexity regions                                     |
| 5. Number of interaction partners                                       |
| 21 [16]                                                                  |
| 1. Single residue composition: I, T, Y                                  |
| 2. Combined amino acid compositions: KR, DE, DENQ                        |
| 3. Predicted secondary structure composition: α and coil                |
| 4. Presence of signal sequence                                           |
| 5. Amino acid sequence length                                            |
| 6. Number of amino acids in both short and long low complexity regions (over sequence length) |
| 7. Normalized low complexity value for both short and long regions (over sequence length) |
| 8. Minimum GES hydrophobicity score calculated over all amino acids in a 20 residue sequence window |
The learning algorithm (i.e. the classification method) is selected based on numerous factors, such as the number of existing examples in the dataset, the data type to be classified (e.g. symbolic or numeric), and the number of examples probable to be inaccurate or noisy. The level of preferred interpretability of the outcomes is another issue to be considered [16].

The majority of current methods use SVM to build the model of solubility [4]. Appropriate SVM models can often achieve better performance in classification of biological sequence compared to other machine learning-based approaches [1]. Each study employs a different set of features. Considering the model performance, different results are obtained, but 70% is a common accuracy in many studies [4].

To date, all of the prediction approaches examined a single system of protein expression, such as the A. niger or the E. coli system. The works of Hirose et al. [3,10] are exceptions that explored two different systems (E. coli and wheat germ).

Some of the suggested methods of prediction offer their work as widely accessible web servers [3,10,17-20]. In spite of more than two decades of research on the subject, there has been only one report, reviewing seven solubility prediction tools [21]. In their valuable review, the authors have compared seven existing prediction tools based on the following factors: prediction accuracy, usability, utility, and prediction tool development and validation methodologies. Our aim is to evaluate and investigate all published methods to predict protein solubility, so as to offer a detailed as well as a general understanding for the researchers.

The organization of the paper is as follows. The major protein solubility prediction studies are reviewed in section 2, with emphasis on their datasets, features, feature selection methods, predictor models and performance results. Section 3 presents a discussion on the models details, the best models and the data challenge for solubility prediction task. Lastly, section 4 concludes the paper and proposes some future research directions.

**Review**

The methods to predict solubility of protein based on the machine learning are summarized in Table 1 in a chronological order, descending from the most recent. Due to space limitation, the reported performance of the works and the features used in each work are shown in Table 2 and Table 3 respectively. More detailed descriptions of the works are presented in "Additional file 1".

In the following tables, for an entry which does not have the corresponding column value, symbol "-" is used. For an entry which we could not find its value, but may exist, symbol "N/A" is used (N/A: Not applicable, not available or no answer).

In order to comprehend the details of the works which are presented in Table 1, Table 2 and Table 3 respectively. More detailed descriptions of the works are presented in "Additional file 1".

In order to comprehend the details of the works which are presented in Table 1, Table 2 and Table 3, datasets used, feature selection methods and performance measures are described in greater details in Table 4, Table 5 and Table 6 respectively.

It should be mentioned that in some works several modeling techniques are examined and then one or more are selected as the final model(s). In the “Modeling Technique(s)” column of Table 1, only the final models are shown. It is same true for the "Feature Selection
| #  | Name            | Reference | Size     | Soluble | Insoluble | Description                                                                 | URL                                      |
|----|-----------------|-----------|----------|---------|-----------|------------------------------------------------------------------------------|------------------------------------------|
| 1  | Sd957           | [8]       | 957      | 285     | 672       | It is made from 3 previous datasets: Idicula-Thomas et al. [28], Diaz et al. [20] and Chan et al. [1]. | http://icl abl.ife.nctu.edu.tw/SCM/downloads.php |
| 2  | PROSO II        | [6]       | 82,000   | 41,000  | 41,000    | It is made from pepcDB and PDB and has been the largest dataset ever. It is balanced. | http://mips.helmholtz-muenchen.de/proso/Suppl_files.zip |
| 3  | HGPD            | [33]      | 17,821   | N/A     | N/A       | Human full-length cDNA.                                                         | http://www.HGPD.jp                       |
| 4  | eSol            | [25]      | 30,173   | N/A     | N/A       | A database on the solubility of entire ensemble of E. coli proteins based on ASKA library. | http://www.tanpaku.org/tp-esol/index.php?lang=en |
| 5  | Solpro (SOLP)   | [17]      | 17,408   | 8704    | 8704      | It is collected from 4 different sources: PDB, SwissProt, TargetDB and dataset of "Idicula-Thomas, 2006". The sequence redundancy is removed with 25% sequence similarity. It is balanced. | http://download.igb.uci.edu/SOLP.fa      |
| 6  | PROSO           | [19]      | 14,000   | 7000    | 7000      | It is collected by merging 4 datasets: TargetDB, PDB and datasets of "Idicula-Thomas, 2005" and "Idicula-Thomas 2006". | -                                         |
| 7  | pepcDB          | [34]      | N/A      | N/A     | N/A       | It stored target and protocol information contributed by Proteome Structure Initiative centres as well as targets imported from the TargetDB database. Now it has been replaced by TargetTrack. | http://pepcdb.rcsb.org                   |
| 8  | Idicula-Thomas 2006 | [27] | 192      | 62      | 139       | It is collected from the literature.                                           | -                                         |
| 9  | Idicula-Thomas 2005 | [28] | 174      | 41      | 133       | It is collected from the literature.                                           | -                                         |
| 10 | PDB             | [35]      | 91,359   | N/A     | N/A       | It is a repository of information about the 3D structures of large biological molecules, including proteins and nucleic acids. | http://www.rcsb.org/pdb/                  |
| 11 | SPINE           | [16]      | N/A      | N/A     | N/A       | N/A                                                                           | http://spine.nesg.org/user_login.cgi?url=http://spine.nesg.org/front_page.cgi? |
Method(s) column. In addition, in most of the works, first an initial feature set is considered, and then using feature selection methods, a smaller sub-set is obtained and employed in the modeling. Table 3 presents the final sets used in the modelings.

With respect to the data used in each study, some of the authors created a dataset harvested from the literature, some employed public datasets, while others performed experiments to generate their own dataset.

Discussion
This section investigates the works in more depth. In the following paragraph, the most used dataset, features, feature selection methods and learning techniques are presented. Afterwards, the best models based on the obtained accuracies are introduced. Then, the most convenient to use models are mentioned. Lastly, some data-related challenges are discussed.

In terms of data, eSol is the most widely used dataset in the field. Considering input features, the following features are the most common ones computed from the protein sequence: aliphatic index, amino acid sequence length, charge, amino acid compositions, instability, isoelectric point (pl), hydrophilicity, molecular weight, and predicted secondary structure. Filter methods (described in Table 5) are used more than the other feature selection techniques. Regarding the machine learning method, support vector machine is the most common technique to make prediction; random forest, decision tree and logistic regression are the next most common ones, respectively.

Based on the results, the method reported by Diaz et al. [20] obtained the best prediction accuracy (94%) on their generated dataset. Similar prediction accuracy was also reported by Samak et al. [4] with an accuracy of 90% on the eSol dataset, followed by the works of Xiaohui et al. [7], and Wilkinson and Harrison [9] with a prediction accuracies of 88% based on their generated datasets.

Comparing the different models in terms of convenience and ease of use, the ones with publicly accessible web servers can be considered the most convenient to use and evaluate. They are ProS [5], PROSOII [6], SCM [8], ESPRESSO [10], SOLpro [17], PROSO [19] and the model of Diaz et al. [20].

It seems that by using an appropriate dataset, as well as suitable machine learning techniques, reasonable prediction performance is attainable. In addition, feature selection methods can reveal, to some extent, influential factors on solubility and the sequence characteristics that could be modified in optimization.

Poor generalization ability is one of the limitations of sequence-based methods founded on a small dataset [35]. In general, extracting a reliable dataset, in terms of experimental conditions and expression system is challenging as the majority of databases that deliver the information on the solubility of proteins often do not provide comprehensive information about the experimental particulars of solubility assessment. Furthermore, researchers generally handle imbalanced (i.e. unequal number of soluble and insoluble samples) data when collecting protein solubility records. Consequently, numerous research teams used different methods to collect consistent datasets that divide proteins into insoluble and soluble categories [24,27].

It is worth mentioning that the datasets employed to build SOLpro [17] and PROSOII [6] were gathered by

| Method | Description | Examples |
|--------|-------------|----------|
| Filter | Filter methods evaluate the relatedness of features by looking at the inherent properties of the data. Usually a feature relevance score is computed, and the features with low scores are discarded. | Student’s t-test [N/A] Information gain [38] Gain ratio [38] Chi squared [N/A] Symmetrical uncertainty [39] Unbalanced correlation score [40] Mann–Whitney test [41] Linear correlation coefficient [N/A] |
| Wrapper | In wrapper methods various subsets of features are evaluated by training and testing a specific classification model, so a search algorithm is ‘wrapped’ around the classification model. This approach adapted to a specific classification algorithm. | Sequential forward selection [42] Sequential backward elimination [42] Beam search [43] ReliefF [44] |
| Embedded | Embedded methods, build the search for an optimal subset of features into the classifier construction, so they are specific to a given learning algorithm. | Random forest [45] SVM recursive feature elimination (SvmRfe) [46] One attribute rule [47] |
integrating different search results of TargetDB, Protein Data Bank (PDB), and Swiss-Prot database. Then, the proteins were categorized into insoluble and soluble samples according to the proteins’ annotations. Although these methods were best working when an appropriate experimental dataset did not exist, they might not be reliable completely. A soluble protein without appropriate annotation, for example, may be incorrectly categorized as an insoluble protein and vice versa. Furthermore, annotations from diverse databases may not be consistent. Clearly, it is desirable to have a large protein set with solubility determined based on experiment by a single reliable protocol [5].

### Conclusions

In this paper, the works to predict protein solubility prediction are reviewed in details. They are assessed and classified with regards to the datasets used, features used, feature selection methods, machine learning algorithms and performance results.

Since the early work of Wilkinson and Harrison [9], models later proposed became more complex in terms

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**Table 6 Performance measures used to evaluate protein solubility prediction (in alphabetical order)**

| #  | Name                  | Abbr. | Formula | Description |
|----|-----------------------|-------|---------|-------------|
| 1  | Accuracy              | ACC   | (TP + TN)/(TP + TN + FP + FN) | The number of correctly classified instances divided by the total number of instances [6]. |
| 2  | Area under ROC curve  | AUC   | -       | It measures the discriminating ability of the model and it takes values between 0.5 for random drawing and 1.0 for perfect classifier [6]. |
| 3  | Enrichment Factor     | EF    | [CS/(CS + WS)]/[S/(S + I)] | EF is especially suitable for the unbalanced datasets [27]. |
| 4  | False Negative        | FN    | -       | The number of incorrectly predicted negatives [10]. |
| 5  | False Positive        | FP    | -       | The number of incorrectly predicted positives [10]. |
| 6  | F-Score               | FS    | 2 × Precision × Recall/(Precision + Recall) | The harmonic mean of recall and precision [10]. |
| 7  | Gain                  | GAIN  | -       | It is an important performance measure that quantifies how much better the decision is in comparison with random drawing of instances [6]. |
| 8  | Matthew’s Correlation Coefficient | MCC | (TP × TN – FP × FN)/((TP + FP)(TP + FN)(TN + FP)/(TN + FN)) | It indicates the correlation between the classifier assignments and the actual class in the two-class case. It is a good measure of classifier performance even when classes are unbalanced [6]. The MCC ranges between −1 and 1, and a large positive value indicates a better prediction [10]. |
| 9  | Precision (Selectivity) | PRC | TP/(TP + FP) Or TN/(TN + FN) | The ratio of the number of correctly classified positive or negative instances to the number of all instances classified as positive or negative, for positive and negative class respectively [6]. |
| 10 | ROC Curve             | ROC   | -       | The receiver-operator characteristic curve, showing the trade-off between the ratio of false positives and false negatives in testing a classifier [48]. A larger area value indicates a more robust prediction method [10]. |
| 11 | Recall (Sensitivity)  | REC   | TP/(TP + FN) | The ratio of the number of correctly classified positive instances to the number of all instances from the positive class [6]. |
| 12 | Specificity (TN-rate) | SPC | TN/(TN + FP) | The ratio of the number of correctly classified negative instances to the sum of all negative instances [6]. |
| 13 | True Positive         | TP    | -       | The number of correctly predicted positives [10]. |
| 14 | True Negative         | TN    | -       | The number of correctly predicted negatives [10]. |

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a. "TP" = True Positive; "TN" = True Negative; "FP" = False Positive; "FN" = False Negative; "+" = Add, ";-" = Subtract; "×" = Multiply; "/" = Division.
of dataset size, number and types of features employed, feature evaluation techniques and machine learning methods to make prediction. In general, the performances of the models have improved greatly as well.

Some of the models provide acceptable prediction performance (e.g. in terms of accuracy). Especially the ones with convenient user interfaces (e.g. web applications), can be considered valuable tools to anticipate recombinant protein overexpression results before performing real laboratory experiments. This capability will lead to significant reduction of labour, time and cost.

Generating larger and more accurate datasets, working on organisms other than *E. coli* and discovering other influential features, are some considerations for future directions in the protein solubility prediction field.

### Additional file

**Additional file 1:** In detailed descriptions of 24 studies to predict protein solubility during 1991–2014 (February).

**Competing interests**
The authors declare that they have no competing interests.

**Authors’ contributions**
NH carried out the literature review studies and drafted the manuscript. SZMH and MRS conceived the idea of the study, and helped to draft the manuscript. NH revised and approved the final manuscript.

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