Abstract: I present new results about the structure of a wide class of infinite groups which were obtained in collaboration with Jesse Peterson (Berkeley). Using L2-cohomology and bounded cohomology we obtained strong results about the subgroup structure of groups with homological properties that resemble negative curvature. These results generalize several central results in geometric and combinatorial group theory.