An attraction–repulsion transition of force on two asymmetric wedges induced by active particles

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Effective interaction between two asymmetric wedges immersed in a two-dimensional active bath is investigated by computer simulations. The attraction–repulsion transition of effective force between two asymmetric wedges is subjected to the relative position of two wedges, the wedge-to-wedge distance, the active particle density, as well as the apex angle of two wedges. By exchanging the position of the two asymmetric wedges in an active bath, firstly a simple attraction–repulsion transition of effective force occurs, completely different from passive Brownian particles. Secondly the transition of effective force is symmetric for the long-range distance between two asymmetric wedges, while it is asymmetric for the short-range case. Our investigations may provide new possibilities to govern the motion and assembly of microscopic objects by taking advantage of the self-driven behaviour of active particles.

Differently from passive Brownian particles, active particles (also known as self-propelled particles) may acquire energy from external source and drive themselves far away from equilibrium. Examples of active matter can be found in various systems ranging from bacteria1,2, algae3,4, spermatozoa5,6, macroscopic animals7,8 to artificial micro-swimmers9–12. Meanwhile active particles exhibit spatiotemporal active states, such as swarming13–15, and turbulence(swirling)16–18. Therefore, researches on the nonequilibrium dynamics of active particles have great significance in not only clarifying its physical mechanisms19–23 but also understanding the natural biological systems, such as bacterial colonies, fish schools, bird flocks24 and so on. Additionally, active particles with a proper design can be widely applied in a variety of areas, such as drug delivery in medicine25,26, gene therapy27, nanoscale assembly28,29, pollution management30, etc.

Passive objects or rigid obstacles immersed into an active bath can guide and accumulate active particles31–34, as well as be taken as trapping devices for active swimmers35–37. Conversely, active swimmers placed by fixed boundaries would undergo a rectification38,39 and sorting40–42 effect. Perhaps the most remarkable phenomenon is that active particles tend to accumulate at the fixed boundaries due to the reduction of its mobility in the proximity of the fixed boundaries. This creates positive feedback corresponding to the motility-induced phase separation (MIPS) between dense and dilute fluid41–45: active particles accumulate where they move more slowly, while steric hindrance or repulsive interactions slow down active particles at high density. Solon et al. successfully introduced an effective free-energy to describe MIPS as a spinodal decomposition in terms of density-field48. MIPS can lead to cohesive active matter in the absence of cohesive forces and the phase-coexistence of active particles displays several relevant differences from the liquid–gas phase coexistence of passive particles49,50. Sandal et al. found that active particles can self-organize into two coexisting phase at different kinetic temperatures, and they are separated from each other by a sharp and persistent temperature gradient50. Ray et al. observed that a robust attractive force appears between two parallel rods immersed into a bath of run-and-tumble active particles, which results from a depletion of active particles in the confinement between two rods by the combined effect both particles swimming along the rods and a geometric shadowing effect. Their results also give a fact that objects can experience a great variety of fluctuation-induced forces in active particles system33. Kaiser et al. showed that a static chevron-shape boundary would represent an excellent trapping device for active particles, and the trap efficiency behaves a phase transition corresponding to three states: partial trapping, complete trapping, no trapping, which is determined by the apex angle of the trap36. Kaiser et al. also experimentally focused on the motion of a pair of symmetrical micro-wedges submersed in a turbulent rod-like bacteria bath. They observed that two micro-wedges of same orientation move such that their mutual distance decreases, while they
drift apart for an anti-parallel orientation. In our recent work, we explored the collective behaviours of active rod-like particles in two symmetrical micro-wedges of anti-parallel orientation using computer simulations. A transition from repulsion to attraction occurs by varying both apex angles of two wedges, which is also sensitive to the particle density. The optimal apex angle \( \theta^* \) and particle density \( \rho^* \) is characterized by the saturated trapping of active particles inside wedge.

Due to the intrinsic non-equilibrium property of active particles, it is interesting to study the non-equilibrium behaviours of active swimmers in a system immersed by an array of asymmetric barriers. The motion of active particles can be rectified in the presence of funnel-shaped obstacles and a ratchet effect is observed even in the absence of an external drive. Volpe et al. found that active swimmers would be sorted with the use of a periodic array of convex obstacles (ellipses). According to these investigations, the asymmetry of obstacles also plays a crucial role in the occurrence of these phenomena, which originates from the broken time symmetry in particle-obstacle interactions. In fact, as we know, in active particle system, the ratchet phenomenon demands two ingredients which are (a) fluctuating input zero-mean force: it should break the thermodynamical equilibrium, and (b) asymmetry (temporal and/or spatial): it can violate the left–right symmetry of the response. In this paper, two asymmetric wedges are immersed in a bath of active rod-like particles, which are taken as the trap device, and our aim is to investigate some special non-equilibrium properties of asymmetric obstacles in an active particle bath. We monitor the directed collective behaviour of active particles near the wedges with variable wedge-to-wedge distance, active particle density, and apex angles of wedge. The final focus is on the attraction–repulsion transition of effective force between two asymmetric wedges. By exchanging the position of the two asymmetric wedges, the attraction–repulsion transition of effective force occurs and this transition is symmetrical at long-range distance, while it is asymmetrical at short-range distance.

**Model and methods**

In our simulation, two asymmetric hard wedges in a suspension of a two-dimensional active bath are considered, shown in Fig. 1. The active bath is modelled by \( N \) rod-like self-propelled particles. Each rod-like particle with length \( l = \sigma \) and width \( d = 0.5\sigma \) consists of three spherical beads, which are equidistantly positioned with a displacement \( S = 0.25\sigma \), along the main rod axis. Here \( \sigma \) is the reduced unit of length. The particle density \( \rho \) is defined by the ratio of the area occupied by \( N \) self-propelled particles to the total area of the system, which can be freely controlled by varying \( N \). The related aspect ratio of the active particle is denoted as \( p = l/d \) (i.e., the length and width of the active particle are \( l \) and \( d \), respectively), and here \( p = 2.0 \), which is the same as that considered in our previous work. Initially, active rod-like particles are placed randomly in the system. Simulations are performed on the boxes of size \( L_x = 200\sigma \) and \( L_y = 100\sigma \) with Periodic Boundary Condition in x- and y-directions, and two hard wedges are embedded in the active bath. We focus on the case of two wedges with same orientation of different apex angles, \( \theta_1 \) and \( \theta_2 \) (varying from 0° to 180°), particle density, \( \rho \), and distance, \( r \). Here \( r \) is defined as the nearest distance between two wedges in x direction, which is not the distance between two cusps of wedges shown in Fig. 1b. Each wedge with length \( L = 20.5\sigma \) and width \( d = 0.5\sigma \) is discretized into 81 spherical beads equidistantly distributed, with a displacement \( S = 0.25\sigma \).

Any overlap of particle–particle or particle-wedge is prohibited by choosing a shifted and cut-off Lennard–Jones potential,

\[
U(R) = \begin{cases} 
4\varepsilon \left[ \left( \frac{\sigma}{R} \right)^{12} - \left( \frac{\sigma}{R} \right)^{6} + \frac{1}{4} \right] & \quad 0 < R \leq 2^{1/6}\sigma \\
0 & \quad \text{otherwise}
\end{cases} 
\]  

![Figure 1. Simple model of two asymmetric wedges in a 2D active bath.](image)
where R is the distance between any two beads (particle–particle or particle-wedge), and ε = 1.0k_BT. Here k_B is the Boltzmann constant and T is the temperature. Active particles swim in a low Reynolds number regime, and the dynamics of the i-th active particle is described by the translational velocity $v_i$ and the angular velocity $w_i$, obeying the following equations:

$$v_i = M_i F_i,$$

$$w_i = K_i T_i,$$

where

$$M_i = m_i \hat{e}_i + m_\perp (E_3 - \hat{e}_i \hat{e}_i),$$

$$K_i = k_i \hat{e}_i + k_\perp (E_3 - \hat{e}_i \hat{e}_i)$$

are the translational and rotational mobility matrices, respectively, and $E_3$ represents the identity matrix. In planar geometry, $k_{\parallel}$ has no contribution in the equations of motion, and mobility value for $k_{\perp}$ is set at 4.8. Translational diffusion coefficient $m_\perp$ is subjected to the aspect ratio of particle p, and here $m_\perp = 0.8452$ for p = 243,48,62–64. The self-propulsion contribution to the total force $F_i$ is $f_0 \hat{e}_i (1 - \theta_i)$, where $f_0$ corresponds to the magnitude of the self-driving force and $\theta_i$ represents the dichotomous state variable, which turns from the value 0 to 1 with the rate $\lambda$ stochastically. Here, $\theta_i = 0$ and $\theta_i = 1$ are indicated as two states, corresponding to the running state and the tumbling state, respectively59,60. During the tumbling state, the total torque $T_i$ receives a random contribution $T_i \theta_i$ that changes the free swimming direction of the active particles59,60, and the tumbling rate is fixed at $\lambda = 0.1$.

In our simulation, all quantities are reported in reduced units ($\sigma = 1$, $m_\parallel = 1$, $k_BT = 1$, and $f_0 = 1$) and are chosen to be the units of length, mass, energy, and force, respectively. The time step is $\Delta t = 10^{-4}$, and each simulation runs from $5 \times 10^7$ up to a maximum of $10^8$ steps. To identify the steady-state, we average the relevant physical quantities over exponentially increasing time windows, and we use this time binning procedure to assess convergence to the steady state65. All statistical properties are averaged over 50 runs. Generally, the magnitude of the self-driving force is $f_0 = 1.0$ except special declaration.

The effective average forces $F(r)$ between the two wedges immersed in the active bath are calculated by the total forces of the wedges exerted by the active particles. Here we only consider the horizontal direction average effective force because of the symmetry of the upper and lower parts of each wedge. The effective forces $F(r) > 0$, $F(r) < 0$, and $F(r) = 0$ represent three interaction states between two asymmetric wedges, corresponding to repulsion, attraction and no interaction, respectively.

**Results and discussion**

**Attraction–repulsion transition for asymmetric wedges.** We first investigate the effective force $F(r)$ between two asymmetric wedges as a function of $r$ at a fixed particle density of $\rho = 0.075$, considering two types of wedges, i.e., Model I ($\theta_1 = 165^\circ$ and $\theta_2 = 90^\circ$) and Model II ($\theta_1 = 90^\circ$ and $\theta_2 = 165^\circ$), as shown in Fig. 2. The interactions of active particles with the wedges are accounted through the potential $U_{\text{total}} = U_1(r_1 - r_L) + U_2(r_1 - r_R)$, where $U_1$ and $U_2$ are the contributions from the left and right wedges, which are given by Eq. (1), respectively, $r_1$ and $r_L$ are the points located long the longitudinal axis of the left and right wedges that are closest to the i-th active particles, respectively62. Therefore, the effective force $F(r)$ is the relative force between two wedges, which is defined as

$$F(r) = F_{12} - F_{34}.$$
The effective force $F(r)$ between two wedges always is attractive, as shown in Fig. 2 (curve in red), which is completely different from Model I. For $0.8 < r < 3$, the attractive force $F(r)$ oscillates as $r$ increases due to the oscillation of particle concentration between the inside and outside of the two wedges. These oscillation behaviours for effective forces are always observed in non-equilibrium system, especially for short-range distance$^{43,63}$. For $r = 1.1$ shown in Fig. 3a-A′, a large cluster is formed near the entrance of the confinement area. As the repulsive part induced by internal particles is slightly less than the attractive part contributed by the particles in the inner contour of right wedge, a weak attraction occurs between two wedges. Compared with $r = 1.1$, as the distance $r$ is increased to $r = 1.2$ shown in Fig. 3b-B′, the dynamic cluster disappears, and few particles can migrate into the cusp of the left wedge while most particles are captured by the right wedge. There is a maximal attractive force due to the great difference on the particle number captured by two wedges. For the case of $r = 3.0$, a few active particles enter the cusp of left wedge, reducing the particle concentration difference between two regions. That's the reason why the attractive force $F(r)$ for $r = 3.0$ is weaker than that for $r = 1.2$. Further, for $r > 3.0$, attractive force decreases firstly, and then keeps unchanged with increasing $r$. Obviously, as the distance is further enlarged, more particles are captured by the left wedge, which leads to the decrease of concentration difference between two regions. When concentration difference reaches the minimum, the attractive force arrives at the minimal.
value and then remains constant. For \( r = 13.0 \) as shown in Fig. 3b-D′, the wedge is driven from their respective active particles gathered inside the wedge. As the particle number in the inner part of right wedge is obviously higher than that of left wedge, the effective force is attractive. As further increasing \( r \), the attractive force would be constant, which is contrary to the case shown in Fig. 3a-D.

In fact, the effective force between two asymmetric wedges is also influenced by the self-driving force \( f_0 \). As shown in Fig. 4, for a larger self-driving force \( f_0 = 3 \), the periodicity of oscillations is the same as in the case of \( f_0 = 1 \), while collisions of active particles with the wedges are more frequent, leading to a great oscillation amplitude of force \( F(r) \) compared to the case of \( f_0 = 1 \). Ni et al. found that both the strength and range of the effective forces between two parallel rods dramatically increase with the increase of self-driving force \( f_0 \). Here our results are also in good agreement with their results. In addition, the effective force between two wedges is also related to the aspect ratio of active particle, \( p \), and the detailed discussions are given in the Supplementary Information.

Figure 3. Density distributions of active particles for Model I- (a) and II-wedges (b) at different distances \( r \).
Effects of particle density. In this section, we will consider the effects of particle density on effective force between two asymmetric wedges. It can be found that the particle density $\rho$ plays an important role in determining the direction and strength of the effective force. We first focus on Model I and show the interaction between two wedges versus $r$ for different particle densities $\rho$, as shown in Fig. 5. In detail, for $\rho = 0.075, 0.1, \text{ and } 0.2$, effective force $F(r)$ experiences a repulsive-attractive-repulsive transition as $r$ increases, while it undergoes the repulsive-attractive transition for low densities of $\rho = 0.01$ and 0.025. For all $\rho$, the effective forces $F(r)$ oscillate firstly at short-range distance, and then achieve stably at long-range distance. For short-range distance, we pick the first peak of effective force $F(r)$ curves for different $\rho$ to display the density distribution of active particles in the left column of Fig. 6. For a low density of $\rho = 0.01$, as shown in Fig. 6a, a dynamic particle bridge forms between two wedges while only a few particles are captured by the inner contour of the right wedge, inducing the two wedges to repel with each other. With increasing particle density from $\rho = 0.01$ to 0.025, 0.075, and even 0.1, as shown in Fig. 6b–d, more particles swarm into the confinement area between two wedges for high density. The difference of particle concentration between inside and outside of two wedges increases, so the repulsive force between two wedges gets larger. Interesting, for a higher density of $\rho = 0.2$, the effective force $F(r)$ between two wedges decreases. It indicates as the inner area of each wedge has reached saturation, further increasing $\rho$ instead weakens the effective repulsive force $F(r)$, see Fig. 6e.

For long-range distance, we choose $r = 13.0$ to compare and the results are shown in the right column of Fig. 6. As $\rho = 0.01$, Fig. 6f shows that a few of particles are preferentially gathered in the cusp of the right wedge, while almost no particle is captured by the left wedge, therefore, interaction force between two wedges is weakly attractive. Increasing particle density from $\rho = 0.01$ to 0.025, as shown in Fig. 6g, more particles are found in the cusp of right wedge, and still only few particles are located in the inside surface of left wedge. The difference of
Figure 6. Density distribution of active particles for Model I-wedges at short-range distance (a) – (e) \((r=1.0)\) and long-range distance (f) – (j) \((r=13.0)\) with different \(\rho\).
particles are also gathered in the left side of each wedge, which then weakens the effective repulsive force $F_2$. This destroys the collective structure of the outer layer in the cusp of the left wedge, see Fig. 6i, j. Meanwhile, some active particles are also gathered in the left side of each wedge, which then weakens the effective repulsive force $F_2$.

For Model II, it is equivalent to exchange the position of the two wedges directly corresponding to Model I. As shown in Fig. 7, for $\rho = 0.01$, two wedges have no interaction for $r < 3.0$ as no particles are captured by wedge, and then repel with each other for $r > 3.0$ due to a few of particles are trapped preferentially by left wedge with $\theta_2 = 90^\circ$. Increasing the particle density from $\rho = 0.01$ to 0.025, 0.075, 0.1 and even 0.2, the effective force oscillates and remains constant with $r$, which is similar to the case of Model I shown in Fig. 5. The oscillation of interaction at short-rang distance results from the oscillation of particle concentration difference between inside and outside of two wedges. For $\rho = 0.025$, the attractive force $F(r)$ increases compared with $\rho = 0.01$ at $r < 3.0$ because more particles are trapped by right wedge, and a transition from attraction to repulsion appears at $r > 10.0$. The transition from attraction to repulsion suggests that more particles are trapped by left wedge as increasing $r$. Further increasing $\rho = 0.075$ enhances the strength of the effective force, because the number of particles trapped by wedge increases with $\rho$ increasing. For a higher particle density $\rho = 0.1$ and 0.2, the effective force decreases as $\rho$ increasing. As the number of particles trapped by wedges has arrived at saturation, increasing $\rho$ would reduce the difference of particle concentration between inside and outside of two wedges.

To explore the relationship between the effective force $F(r)$ and the particle density in more detail, we calculate the effective force $F(r)$ as a function of $\rho$ for Model I- and II-wedges. We first discuss the case of long-range distance ($r = 13.0$) shown in Fig. 8a. For Model I, a transition from attraction to repulsion occurs with increasing $\rho$. There are two critical points (about at $\rho_1 = 0.025$ and $\rho_2 = 0.06$). The attractive force increases as the number of particles trapped by the right wedge with $\theta_2 = 90^\circ$ get larger with increasing $\rho$. Then the attractive force decreases to zero and reverse to repulsive force as more particles are captured by left wedge with $\theta_1 = 15^\circ$, and the left wedge also gets saturation corresponding to the second critical point ($\rho_3 = 0.06$). Here two critical particle densities ($\rho_1 = 0.025$ and $\rho_2 = 0.06$) occur in the dilute regime, which are also consistent with the studies by Kaise et al.36 For a higher particle density ($\rho = 0.1$ and 0.2), more particles swim outside of two wedges, reduce the particle concentration difference between inside and outside of two wedges, and weaken the repulsive force between two wedges. Although the apex angle $\theta$ of the wedges plays a key role in determining the trapping efficiency of wedge, the total number of active particles trapped by the wedge also relies on the particle density $\rho$ of active particles. Symmetrically, for Model II, there is a transition from repulsion to attraction with increasing $\rho$. To clarify the underlying mechanism of this behaviour caused by particle density, we explore the independent force exerted by active particles of each side of two wedges, where the results are shown in Fig. 9. Figure 9a shows that for low particle densities such as $\rho < 0.025$, there are more active particles gathered in the cusp of the right wedge than the left one, which leads to a fact that $F_2$ is always close to 0, and $F_4$ increases abruptly with particle density increasing. However, for $\rho > 0.025$, active particles are gathered massively in the cusp of the left wedge and $F_4$ increases more greater than $F_2$, which leads to the maximum of the difference between $F_4$ and $F_2$ at $\rho = 0.060$. As known, there are different collective abilities for the wedges with different angles of $\theta_1 = 15^\circ$ and $\theta_2 = 90^\circ$. When $\rho$ increases further, $F_4$ increases slowly and the right wedge reaches saturation finally. However, $F_2$ drops slowly instead because the overflowing particles would collide and even disturb the collective layer of the left wedge. Caprini and Marconi have investigated the effects of geometric confinement on the steady-state properties of a one-dimensional active suspension subject to thermal noise, and the random active force on the confining wall is studied both numerically, by integrating the Langevin governing equations, and analytically by solving the associated Fokker–Planck equation under suitable approximations. They obtained a non-uniform density profiles because active particles accumulate near the wall, and the force exerted on the wall depends on

![Figure 7. Effective force $F(r)$ between two wedges as a function of $r$ for Model II-wedges with different $\rho$.](https://doi.org/10.1038/s41598-020-68677-w)
the wall separation. Inspired by their work, we also calculate the independent force exerted on two sides of each wedge, explaining the attraction–repulsion transition of effective force between two asymmetric wedges. The force acting on the wedge originates from the average collision of active particles, and the underlying mechanism attributes the accumulation to the reduction of the active particles' mobility in the presence of the wedges.

Then consider the case of short-range distance (r = 1.0) shown in Fig. 8b, differently from the long-range distance. For Model I, the repulsive force increases first and then decreases with increasing particle density ρ shown in Fig. 8b. Meantime, Fig. 9c, d show how the independent forces rely on the particle density ρ. With a low ρ, few particles are found in the confinement of two wedges. As increasing ρ, more particles flock into the confinement area, which is also reflected by the rapid growth of F2 and F3 shown in Fig. 9c, and leads to the increase of the repulsive force between two wedges. Once the number of particles trapped in the confinement achieves saturated, further increasing ρ would reduce the independent forces of F2 and F3 because more active particles can destroy the collective structures of active particles in the outer layer, which weakens the repulsive force a little. This result originates from the instability of trapping of active particle, which agrees well with the Kaiser's results36,66,68. However, for Model II, two wedges attract first and then repel with each other with increasing ρ, different from the case of Model I. At a low particle density (ρ < 0.06), with increasing ρ, more and more particles are captured by right wedge, and the attraction gets stronger. As ρ > 0.06, more particles run into the confinement area, the attractive force is decreased to be zero and then reversed to repulsive force. From Fig. 8, we can conclude that by exchanging the position of the two asymmetric wedges, the transition of effective forces is symmetrical at long-range distance, while symmetry destruction occurs in short-range situations. Different behaviour for effective force between two asymmetric wedges at the long-range and short-range distances represents a typical ratchet phenomenon in active particle system in which it breaks the thermodynamical equilibrium, as well as it violates the left–right symmetry38,51,52,54.

Effects of the apex angles of wedge. Finally, we investigate the effects of wedge shape on the interaction between two wedges. Here, we underline the asymmetric transition of the effective force at short-range distance and symmetric transition at long-range distance as a response to the interchange of two wedges positions, and
The results are shown in Fig. 10. At long-range distance (r = 13.0) shown in Fig. 10a, the effective force displays symmetry for both cases: θ₁ variable with θ₂ = 90°, and θ₁ = 90° with θ₂ variable. For the former, an attraction–repulsion transition occurs as θ₁ increases from θ₁ = 0° to 180°. For a small angle (θ₁ = 5°), most active particles are collected by the right wedge, while hardly any particles are captured by the left wedge, leading to an attraction between the two wedges. Increasing θ₁ from θ₁ = 5° to 90°, the trap efficiency of the left wedge improves, which would diminish the difference in the number of particles captured by the two wedges and weaken the attraction. Similarly, increasing θ₁ from 90° to 165°, more particles are trapped by the left wedge until the trap efficiency is maximized. Further increasing θ₁, the trap efficiency of the left wedge declines, which can lead to an attraction interaction between the two wedges. As shown in Fig. 10b, one apex angle of two wedges is fixed at θ = 165°. For θ₁ variable with θ₂ = 165°, the interaction between the two wedges is attractive overall, and the attraction increases and then decreases as θ₁ increases. There is an optimal angle of θ₁ = 165°, in which the trap efficiency reaches a maximum and two wedges have no interaction equivalently. In order to unveil the physical reason of the phenomenology observed, we monitor the independent force of each wedge attributed by the collisions between active particles and the wedge, and the results are given in Fig. 11. Figure 11a shows that F₁, F₃, and F₄ keep unchanged, and only the force F₂, acting on the inside surface of the left wedge, varies as the apex angle increases, which leads to a non-monotonic behavior for the effective force F(r) between the two wedges, as shown in Fig. 11b.

In addition, at short-range distance (r = 1.0) shown in Fig. 10c, the effective force shows two distinctive behaviors for both cases: θ₁ = 90° with θ₂ variable, and θ₁ variable with θ₂ = 90°. For θ₁ = 90° with θ₂ increasing from 5° to 60°, the repulsive force increases gradually. At θ₂ = 5°, compared to this narrow angle, part of active particles is prioritized in the cusp of the left wedge, which leads to a repulsive interaction between the two wedges. With increasing θ₂, particles bridges are formed gradually and a greater repulsion is produced. Especially for θ₂ = 90°, few particles can swim into the confinement because the confinement is rather narrow, which results in an attraction. As 90° < θ₂ < 120°, more particles can move into the confinement to enlarge the effective force. For 120° < θ₂ < 165°, due to the trap efficiency of the right wedge improving with the increase of the apex angle, the repulsive force decreases and even turns to be an attraction at θ₂ = 165°. For θ₂ > 165°, the trap efficiency of right

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Figure 9. Independent force F acting on two wedges induced by active particles as a function of ρ for Model 1-wedges: at long-range distance of r = 13.0 (a) and (b), and at short-range distance of r = 1.0 (c) and (d). Here, $F_{12} = F_2 - F_1$, $F_{34} = F_4 - F_3$, and $F(r) = F_{12} - F_{34}$. 
wedge decreases, so that the repulsive force between two wedges gets larger. Conversely, for θ_1 variable with \( \theta_2 = 90° \), a weak repulsion increases first and then decreases at \( 5° < \theta_1 < 90° \), and the effective force increases at \( 90° < \theta_1 < 120° \), then slightly decreases as \( \theta_1 > 120° \). With a very small angle of \( \theta_1 = 5° \), particles cover the left side of the right wedge, so there is a weak repulsive force. Increasing \( \theta_1 \) from 15° to 90°, see Fig. 11c, d, \( F_3 \) decreases as only few particles can stay the left side of the right wedge and \( F_2 \) increases first, then decreases because the inside area of the left wedge gets larger, leading to a reduction of the effective force. For \( 90° < \theta_1 < 120° \), the confinement can accommodate enough particles and strengthen the repulsive force. For \( \theta_1 > 120° \), particles cannot stay in the confinement between two wedges stably for its large area, decreasing the repulsive force. Our result is consistent with the result of Kaiser et al.\(^{36,37,66,68} \), which is that the catching efficiency can be controlled by varying the apex angle of the wedge, and the particle density difference decides the direction and strength of the effective force between the two wedges.

For comparison, we also fix one apex angles of two wedges at \( \theta = 165° \) and the other is variable, as shown in Fig. 10d. For \( \theta_1 = 165° \) with \( \theta_2 \) variable, the repulsive force increases at \( 5° < \theta_2 < 160° \), then decreases at \( 160° < \theta_2 < 165° \), and finally increases at \( \theta_2 > 165° \). For \( 5° < \theta_2 < 160° \), due to the confinement gets smaller, and particles bridges are formed leading to a greater repulsion. For \( 160° < \theta_2 < 165° \), the confinement is too narrow to accommodate many active particles, producing a drop in repulsion. For \( \theta_2 > 165° \), the trap efficiency of right wedge declines, so the repulsive force gets larger. For \( \theta_2 \) variable with \( \theta_1 = 165° \), the attractive force increases during \( 5° < \theta_1 < 120° \), due to the narrow confinement area and the high trap efficiency of right wedge. At \( 120° < \theta_1 < 155° \), dynamic particle bridges are formed between two wedges, which enhances the repulsive force. At \( 155° < \theta_1 < 165° \), the confinement is too narrow to accommodate many active particles, producing a drop in repulsion. At \( \theta_1 > 165° \), particle bridges are formed again in the confinement between two wedges, enhancing the repulsion. Our results suggest the shape of wedge plays a crucial role in determining the trap efficiency, and there are three distinct states: no trapping at wide angles followed by a sharp transition towards complete trapping at medium angles and a crossover to partial trapping at small cusp angles\(^{36} \). We also explore the effective force of two parallel rods (i.e., \( \theta_1 = \theta_2 = 180° \)) in an active bath, and the results are shown in Supplementary Figure S2. Our result is consistent with the Knežević’s work\(^{82} \), and some discussions are given in the Supplementary information.

As a result, by exchanging the position of two asymmetric wedges, the transition of effective forces is symmetric for the long-range distance, while it is asymmetric for the short-range case. The dramatic collective response of active particles to the exchange of two wedges is noteworthy and never discovered in the passive system. We further emphasize the conversion of the interaction orientation is a collective, nonequilibrium behaviour.

Figure 10. The repulsion and attraction force \( F(r) \) between two wedges in an active bath with different types of wedges: the apex angle of the one wedge is fixed: 90° (a and c) or 165° (b and d), and the other one is variable (0° – 180°).
Conclusions

Using computer simulation, we studied the effective interaction between two asymmetric wedges exposed to a bath of active particles. The effective force between two wedges is strongly related to the relative position of two wedges, the wedge-to-wedge distance $r$, the particle density $\rho$, as well as the apex angle of wedge $\theta$ ($\theta_1$ or $\theta_2$). For a set of fixed apex angles with $\theta_1 = 165^\circ$ and $\theta_2 = 90^\circ$, by only exchanging the position of the two asymmetric wedges, the left–right asymmetry due to this exchange and the self-driven behaviour of active particles together cause the two distinct transitions of effective force between two wedges. Further, with the exchange of the two wedge positions, whether it’s changing particle density $\rho$ or apex angle ($\theta_1$ or $\theta_2$), it is found that the effective force shows asymmetry for short-range distance between two asymmetric wedges, while it has symmetry for the long-range case. Our results further reveal that the effective force transition from attraction to repulsion is attributed to a collective, nonequilibrium effect and the self-driven behaviour of active particles. Our investigations may pave a novel way to applications for the design of tunable interactions by using active matter.

References

1. Tailleur, J. & Cates, M. E. Statistical mechanics of interacting run-and-tumble bacteria. Phys. Rev. Lett. 100, 218103 (2008).
2. Peruani, F. et al. Collective motion and nonequilibrium cluster formation in colonies of gliding bacteria. Phys. Rev. Lett. 108, 098102 (2012).
3. Polin, M., Tuval, I., Drescher, K., Gollub, J. P. & Goldstein, R. E. Chlamydomonas swims with two "gears" in a eukaryotic version of run-and-tumble locomotion. Science 325, 487–490 (2009).
4. Ma, R., Klindt, G. S., Riedel-Kruse, I. H., Jülicher, F. & Friedrich, B. M. Active phase and amplitude fluctuations of flagellar beating. Phys. Rev. Lett. 113, 048101 (2014).
5. Riedel, I. H., Kruse, K. & Howard, J. A self-organized vortex array of hydrodynamically entrained sperm cells. Science 309, 300–303 (2005).
6. Friedrich, B. M. & Jülicher, F. The stochastic dance of circling sperm cells: Sperm chemotaxis in the plane. New J. Phys. 10, 123025 (2008).
7.VICEK, T. & Zafeiris, A. Collective motion. Phys. Rep. 517, 71–140 (2012).
8. Cavagna, A. & Giardina, I. Bird flocks as condensed matter. Annu. Rev. Condens. Matter Phys. 5, 183–207 (2014).
9. Golestanian, R., Liverpool, T. B. & Ajdari, A. Propulsion of a molecular machine by asymmetric distribution of reaction products. Phys. Rev. Lett. 94, 228001 (2005).
10. Erbe, A., Zientara, M., Barabán, I., Kreidler, C. & Leiderer, P. Various driving mechanisms for generating motion of colloidal particles. J. Phys. Condens. Matter 20, 404215 (2008).
11. Marchetti, M. C. et al. Hydrodynamics of soft active matter. Rev. Mod. Phys. 85, 1143–1189 (2013).
12. Saintillan, D. & Shelley, M. J. Theory of active suspensions. In Complex Fluids in Biological Systems (ed. Spagnolie, S.) 319–355 (Springer, New York, 2014).
13. Yang, X., Marceau, V. & Gompper, G. Swarm behavior of self-propelled rods and swimming flagella. Phys. Rev. E 82, 031904 (2010).
14. Chen, X., Dong, X., Beér, A., Swinney, H. L. & Zhang, H. P. Scale-Invariant correlations in dynamic bacterial clusters. Phys. Rev. Lett. 108, 148101 (2012).
15. Cohen, J. A. & Golestanian, R. Emergent cometlike swarming of optically driven thermally active colloids. Phys. Rev. Lett. 112, 068302 (2014).
16. Abkhamar, M., Marx, K., Auth, T. & Gompper, G. Collective behavior of penetrable self-propelled rods in two dimensions. Phys. Rev. E 88, 062314 (2013).
17. Drocco, J. A., Olson Reichardt, C. J. & Reichardt, C. Bidirectional sorting of flocking particles in the presence of asymmetric barriers. Phys. Rev. E 85, 056102 (2012).
18. Fily, Y. & Marchetti, M. C. Athermal phase separation of self-propelled particles with no alignment. Phys. Rev. Lett. 108, 235702 (2012).
19. Cates, M. E. Diffusive transport without detailed balance in motile bacteria: Does microbiology need statistical physics? Rev. Prog. Phys. 75, 046201 (2012).
20. Bechinger, C. et al. Active particles in complex and crowded environments. Rev. Mod. Phys. 84, 045006 (2016).
21. Ramaswamy, S. The mechanics and statistics of active matter. Annu. Rev. Condens. Matter Phys. 1, 323–345 (2010).
22. Elgeti, J., Winkler, R. G. & Gompper, G. Physics of microswimmers—single particle motion and collective behavior: A review. Rep. Prog. Phys. 78, 056601 (2015).
23. Romanzcuk, P., Bär, M., Ebeling, W., Lindner, B. & Schimsansky-Geier, L. Active brownian particles. Eur. Phys. J. Spec. Top. 202, 1–162 (2012).
24. Dreyfus, R. et al. Microscopic artificial swimmers. Nature 437, 862–865 (2005).
25. Deng, Z. Y., Zhang, D. & Zhang, L. X. Dynamics of attractive vesicles in shear flow. Chin. J. Polym. Sci. 34, 623–636 (2016).
26. Chen, J. X., Chen, Y. G. & Ma, Y. Q. Chemotactic dynamics of catalytic nanker nanomotors. Soft Matter 12, 1876–1883 (2016).
27. Yang, W., Misko, V. R., Nelissen, K., Kong, M. & Peeters, F. M. Using self-driven microswimmers for particle separation. Soft Matter 8, 5175–5179 (2012).
28. Ghosh, A. & Fischer, P. Controlled propulsion of artificial magnetic nanostructured propellers. Nano Lett. 9, 2243–2245 (2009).
29. Eshultan, B. et al. Motion-based threat detection using microrods: Experiments and numerical simulations. Nanoscale 7, 7833–7840 (2015).
30. Chin, C. D., Linder, V. & Sia, S. K. Lab-on-a-chip devices for global health: Past studies and future opportunities. Lab Chip 7, 41–57 (2007).
31. Denissenko, P., Kantsler, V., Smith, D. J. & Kirkman-Brown, J. Human spermatozoa migration in microchannels reveals boundary-following navigation. Proc. Natl. Acad. Sci. U. S. A. 109, 8007–8010 (2012).
32. Guidobaldi, A. et al. Geometrical guidance and trapping transition of human sperm cells. Phys. Rev. E 89, 032720 (2014).
33. Ray, D., Reichardt, C. & Olson Reichardt, C. J. Casimir effect in active matter systems. Phys. Rev. E 90, 013019 (2014).
34. Fily, Y., Baskaran, A. & Hagan, M. F. Dynamics of self-propelled particles under strong confinement. Soft Matter 10, 5609–5617 (2014).
35. Wensink, H. H. & Löwen, H. Aggregation of self-propelled colloidal rods near confining walls. Phys. Rev. E 78, 031409 (2008).
36. Kaiser, A., Wensink, H. H. & Löwen, H. How to capture active particles. Phys. Rev. Lett. 108, 268302 (2012).
37. Kaiser, A. et al. Transport powered by bacterial turbulence. Phys. Rev. Lett. 112, 158101 (2014).
38. Denisov, S., Hänggi, P. & Mateos, J. L. AC-driven brownian motors: A Fokker–Planck treatment. Phys. Rev. E 88, 042601 (2013).
39. Hulme, S. E. et al. Using ratchets and sorters to fractionate motile cells of Escherichia coli by length. Lab Chip 8, 1888–1895 (2008).
40. Potiguar, F. Q., Farias, G. A. & Ferreira, W. P. Self-propelled particle transport in regular arrays of rigid asymmetric obstacles. Phys. Rev. E 90, 012307 (2014).
41. Costanzo, A., Elgeti, J., Auth, T., Gompper, G. & Ripoll, M. Motility-sorting of self-propelled particles in microchannels. Europhys. Lett. 107, 36003 (2014).
42. Hua, Y. F., Li, K., Zhou, X. L., He, L. L. & Zhang, L. X. An attraction–repulsion transition of force on wedges induced by active particles. Soft Matter 14, 5205–5212 (2018).
43. Restrepo-Pérez, L., Soler, L., Martínez-Cisneros, C. S., Sánchez, S. & Schmidt, O. G. Trapping self-propelled micromotors with microfabricated chevron and heart-shaped chips. Lab Chip 14, 1513–1518 (2014).
44. Kantaler, V., Dunkel, J., Polin, M. & Goldstein, R. E. Ciliary contact interactions dominate surface scattering of swimming eukaryotes. Proc. Natl. Acad. Sci. U. S. A. 110, 1187–1192 (2013).
45. Di Leonardo, R. et al. Bacterial ratchet motors. Proc. Natl. Acad. Sci. U. S. A. 107, 9541–9545 (2010).
46. Wan, M. B., Olson Reichardt, C. J., Nussinov, Z. & Reichardt, C. Rectification of swimming bacteria and self-driven particle systems by arrays of asymmetric barriers. Phys. Rev. Lett. 101, 018102 (2008).
47. Solon, A. P., Stenhammar, J., Cates, M. E., Kafri, Y. & Tailleur, J. Generalized thermodynamics of motility-induced phase separation: Phase equilibria, Laplace pressure, and change of ensembles. New J. Phys. 20, 075001 (2018).
48. Caprini, L., Marconi, U. M. B. & Puglisi, A. Spontaneous velocity alignment in Motility-induced phase separation. Phys. Rev. Lett. 124, 078001 (2020).
49. Sandal, S., Liebchen, B. & Löwen, H. Motility-induced temperature difference in coexisting phases. Phys. Rev. Lett. 123, 228001 (2019).
50. Varzy, E. & Schnitzer, O. Ratcheting of Brownian swimmers in periodically corrugated channels: A reduced Fokker–Planck approach. Phys. Rev. E 90, 032115 (2014).
51. Reichardt, C. & Olson Reichardt, C. J. Active matter ratchets with an external drift. Phys. Rev. E 88, 062310 (2013).
52. Volpe, G., Buttini, I., Vogt, D., Kümmeler, H.-J. & Bechinger, C. Microswimmers in patterned environments. Soft Matter 7, 8810–8815 (2011).
53. Speck, T., Baláž, I., Menzel, A. M. & Löwen, H. Effective Cahn–Hilliard equation for the phase separation of active Brownian particles. Phys. Rev. Lett. 112, 218304 (2014).
54. Redner, G. S., Hagan, M. F. & Baskaran, A. Structure and dynamics of a phase-separating active colloidal fluid. Phys. Rev. Lett. 110, 055701 (2013).
56. Bialké, J., Siebert, J. T., Löwen, H. & Speck, T. Negative interfacial tension in phase-separated active Brownian particles. *Phys. Rev. Lett.* **115**, 098301 (2015).
57. Tailleur, J. & Cates, M. E. Sedimentation, trapping, and rectification of dilute bacteria. *Europhys. Lett.* **86**, 60002 (2009).
58. Cates, M. E. & Tailleur, J. Motility-induced phase separation. *Annu. Rev. Condens. Matter.* **6**, 219–244 (2015).
59. Paoluzzi, M., Di Leonardo, R. & Angelani, L. Self-sustained density oscillations of swimming bacteria confined in microchambers. *Phys. Rev. Lett.* **115**, 188303 (2015).
60. Angelani, L., Leonardo, R. D. & Buocca, G. Self-starting micromotors in a bacterial bath. *Phys. Rev. Lett.* **102**, 048104 (2009).
61. Paoluzzi, M., Leonardo, R. D., Marchetti, M. C. & Angelani, L. Shape and displacement fluctuations in soft vesicles filled by active particles. *Sci. Rep.* **6**, 34146 (2016).
62. Knežević, M. & Stark, H. Capillary condensation in an active bath, arXiv: 1908.10483v1.
63. Ni, R., Cohen Stuart, M. A. & Bolhuis, P. G. Tunable long range forces mediated by self-propelled colloidal hard spheres. *Phys. Rev. Lett.* **114**, 018302 (2015).
64. Angelani, L. & Di Leonardo, R. Numerical modeling of bacteria propelled micromotors. *Comput. Phys. Commun.* **182**, 1970–1973 (2011).
65. Patch, A., Yllanes, D. & Marchetti, M. C. Kinetics of motility-induced phase separation and swim pressure. *Phys. Rev. E* **95**, 012601 (2017).
66. Kaiser, A., Sokolov, A., Aranson, I. S. & Löwen, H. Mechanisms of carrier transport induced by a microswimmer bath. *IEEE Trans. Nanobiosci.* **14**, 260–266 (2015).
67. Caprini, L. & Marconi, U. M. B. Active particles under confinement and effective force generation among surfaces. *Soft Matter* **14**, 9044–9054 (2018).
68. Kaise, A., Sokolov, A., Aranson, I. S. & Löwen, H. Motion of two micro-wedges in a turbulent bacterial bath. *Eur. Phys. J. Spec. Top.* **224**, 1275–1286 (2015).

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Methodology, K.L., F.G., X.Z., and X.W.; supervision, L.H.; validation, K.L.; writing—original draft, K.L. and L.H.; writing—review and editing, L.Z. and X.W. All authors discussed the results and review the manuscript.

**Competing interests**

The authors declare no competing interests.

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