Reconfigurable control as actuator fault-tolerant control design for power oscillation damping

Digvijay V. Nair¹* and MSR Murty²

Abstract

This paper presents design of an self contained actuators unit in wide area damping control of power system in stabilizing system response for both nominal system condition and during actuator faults. First it is presented that use of multiple actuators in wide area control aid in improving damping in power system. A wide area damping controller feeding multiple actuators to satisfy multiple objectives in wide area damping control of power system is designed. Minimization of infinity norm of closed loop transfer function of power system with wide area controller in feedback path & closed loop poles placement techniques are used in controller synthesis. Second a reconfigurable control on the lines of fault hiding principle is added to the controller design to maintain system damping to pre-fault level in case of actuator faults. A reconfiguration component (RC) is activated on occurrence of actuator fault thereby reconfiguring system dynamics and redistributing wide area control signal among remaining active actuators. RC together with remaining active actuators and under same wide area damping controller maintains system damping to pre-fault level thereby preserving system dynamic response. In the reconfigurable control design presented here no new actuators outside the unit of actuators designed for wide area damping control is required. This makes for an self contained actuators unit in wide area damping control of power system both for nominal system condition and for system affected by actuator faults. A two area power system model is considered here for demonstrating effectiveness of designed robust damping controller with multiple outputs feeding multiple actuators in wide area control and illustrating the idea of self contained actuators unit for maintaining system damping in case of actuator faults.

Keywords: Wide area control, Robust damping controller, Actuator fault, Reconfigurable control, Reconfiguration component, Self contained actuators unit, Power oscillations

1 Introduction

One of the major concerns of power system is small signal instability and power oscillations arising out of small changes taking place in power system. Small signal stability is the ability of the system to maintain synchronous operation of generators for constant changes (small in comparison to net generated power in system) in operating conditions of power system. This can be load changes, transmission line outages, generator faults and so on. These constant changes witnessed in power system results in power oscillations mostly of electro-mechanical in nature involving multiple machines within same or different areas exchanging power between them [1]. Local oscillations are damped by control units like power system stabilizers (PSS) but for inter-area oscillations involving generators from different areas is difficult to be damped locally. Local controllers lack global observation to see inter-area modes responsible for power oscillations between machines from different areas [2]. With advent of phasor measurement units (PMUs) involved in synchronised and high speed data measurements and transmission from remote locations is made possible [3, 4]. This solves problem of lack of global observation needed for control action to damp out inter-area oscillations [5]. PMUs led to newer controller designs for wide area damping control of power system [6–8]. Dedicated controllers connecting remote signals to local stabilizing units are
designed as part of wide area control (WAC) and damping of power system. Newer controller design techniques based on remote feedback signals and wide area control inputs capable of robust system performance under wide operating conditions have been made possible [7, 9].

The pace of implementation of wide area control & damping in power system is slow. The reluctance of power companies to do so can be attributed to issues like latency in transmission of wide area signals, insufficient bandwidth & loss of wide area signals [10]. The use of centralized controller in WAC of power system requires highly reliable communications and fast and efficient computations. Signals are transmitted from remote locations to central controller and from there to select reference inputs (actuators) of power system. Any delay in transmission and arrival of signal or loss of link between controller and power system can adversely affect system performance [11].

The development of WAC includes design of supplementary control inputs at excitation system of generators, at reference input of HVDC system & at reference input of FACTS devices. The loss of either of (i) remote signals to controller called as sensor faults or (ii) control signals from controller to system termed as actuator faults, reduces effectiveness of WAC. To gain full benefit of WAC in oscillation damping and improving reliability of it’s operation wide area controller should be cemented further with appropriate fault tolerant control strategy to prevent any deterioration from setting in system response. The issues of loss of remote signals in WAC and it’s effect on system stability was studied and reported in [11, 12]. Few fault tolerant control designs for damping of oscillations in WAC of power system are [13–17]. Sevilla et al. [16] has dealt specifically with sensor faults in WAC and presented fault tolerant controller effective during fault but conservative in action during normal system condition. In [15] design of dynamical block called virtual actuator on occurrence of actuator fault as part of fault tolerant damping controller is presented. Pedersen et al. [13] presents design of VAF as part of fault tolerant emergency control for system stability under sudden loss of actuator in WAC of power system.

In this paper design of self contained actuators unit, a novel concept, in wide area damping control of power system, for maintaining sufficient damping in system under different operating points and at the same time capable of restoring system performance on actuator fault is presented. First the use of multiple actuators in wide area damping control and its effectiveness in increasing damping in system is presented. A wide area robust damping controller (WRDC) with multiple outputs connected to multiple actuators (here called self contained unit of actuators) is synthesized to meet multiple requirements from it like disturbance rejection, control effort optimization & to maintain minimum specified damping in system. The design framework used to realize WRDC is based on linear matrix inequality (LMI) condition. Each LMI corresponds to a constraint imposed on controller. Solving for optimization of defined objective function under given constraints results into controller realization.

Second a reconfigurable control is added to wide area damping controller that on actuator fault activates an dynamical block called reconfiguration component (RC). RC together with remaining active actuators (from the same unit) compensate for loss of control action due to actuator fault. RC redistributes wide area control signal to active actuators left from the unit without need of adding any redundant actuator to the unit. RC is designed to satisfy fault hiding principle that hides the actuator fault from the nominal WRDC. On activation of RC the same nominal WRDC is used in generating control action required for meeting specified minimum damping in system and maintaining system performance post actuator fault. The dependence on actuators from same unit designed for wide area control and damping of power system even in case of actuator faults for maintaining system performance makes for an self contained actuators unit. The unit consisting of multiple actuators involved in wide area damping control with controller (WRDC) becomes self sufficient and sees dynamic allocation of control action among active actuators on actuator faults during control operation. This paper extends [18, 19] from discussing effect of actuator faults on system performance to proposing FTC strategy against actuator fault. In particular this paper extends [15] from single actuator to multiple actuator based wide area control, proposing design of self contained actuators unit independently stabilizing system response on actuator fault without any dependence on redundant actuators unlike in [15].

The rest of the paper is organized as follows: dynamic model representation of components used as actuators in WAC is given in Section 2, in Section 3 robust control design of wide area robust damping controller (WRDC) is given. In Section 4 the proposed concept of self contained actuators unit in wide area control & damping is described and design of reconfiguration component (RC) and its application to WAC of power system is given. In Section 5 study of proposed wide area robust damping controller (WRDC) and reconfigurable control as fault tolerant control methodology on a two area power system is presented with results and discussion. Concluding remarks are made in Section 6.

2 Inputs: wide area control of power system
In this section model representation of components used as possible inputs (actuators) in wide area control of power system is given. The supplementary control input at Generator’s excitation system, FACTS devices like static var
The generator constants \( (2) \). The variables and constants used in (1) & (2) are described in nomenclature. Rotor dynamics of synchronous machine is described in (3) [22]. The supplementary control terminal of HVDC system serves as another possible input point location for wide area control signal. HVDC system is based on line commutated converter. Damping can be increased in power system by modulating the reference current at the input of the rectifier. The dynamics of the modulated DC power by applying wide area control input to the supplementary control terminal of HVDC system is as represented in (5) [15]. The variables and constants used in (5) are explained in nomenclature.

\[
\begin{align*}
\dot{x}_d &= \frac{E_{fd}}{T_A} + \frac{K_A}{T_A} \left[ V_{ref} + V_{pass} - V + V_{mod} \right] \\
\dot{x}_q &= \frac{E_{fq}}{T_A} + \frac{K_A}{T_A} \left[ V_{ref} + V_{pass} - V + V_{mod} \right]
\end{align*}
\]

The supplementary control input in WAC for damping of power oscillations is provided by static var compensator(SVC). The main control objective of SVC is to maintain constant bus voltage. It comprises of thyristor control rectifier(TCR) and fixed capacitor(C). Setting appropriate values of firing angle of TCR, net susceptance\((B_{svc})\) and reactive current by it can be controlled. The dynamic model of SVC used here is given in (4) [23, 24]. The variables and constants used in (4) are described in nomenclature.

\[
\begin{align*}
T_{dc} \frac{dP_{dc}}{dt} &= -P_{dc} + P_{ref} + \text{sat} \left( \frac{P_{mod}}{s} \right)
\end{align*}
\]

### 3 Wide area robust damping controller:WRDC

In this section a wide area robust damping controller (WRDC) for damping of power oscillations is designed. The wide area controller is designed to meet multiple objectives from sensitivity minimization, to attenuate disturbance effects on system output to achieve desired minimum damping in system. The objective of sensitivity minimization in presence of system uncertainties and disturbance attenuation is obtained by minimizing the infinity norm of the closed loop transfer function between output disturbance \(d\) and system input \(u\) as shown in Fig. 1. The second objective of minimum damping in system is obtained by regional closed loop pole placement in conic region in complex plane.

The linear model of nominal system under normal operating conditions is given by (6). It is represented as open loop system(G) in the Fig. 1.

\[
\Sigma_G : \begin{cases} \dot{x} = Ax + Bu + B_dd \\ y = Cx \end{cases} \]

where matrices \(A\), \(B\) & \(C\) are the state matrices of appropriate dimensions depending on system order and number of inputs and outputs. A dynamic controller \((K(s))\) representing WRDC is connected to open loop system\((G(s))\), representing power system. With select output signals of \(G\) as feedback to \(K\) and output of \(K\) to select inputs of \(G\) forms a closed loop system as shown in Fig. 1. The state space model of \(K(s)\) is as given in (7).

\[
\Sigma_K : \begin{cases} \dot{x}_k = A_kx_k + Bu_k \\ u = C_kx_k \end{cases}
\]
The minimization of the matrix inequalities as stated in (11) and (12) act as constraint of an optimization problem. The objective function of which is minimization of scalar \( \gamma_c \) (for \( \gamma_c > 0 \)). The solution to the resultant optimization problem gives controller state matrices \((A_c, B_c, C_c)\) along with the matrix \( \hat{Q} \) \([25, 26]\).

4 Proposed FTC design of self contained actuators unit:

In this section the concept of self contained actuators unit as actuator fault-tolerant control design is discussed. In wide area control and damping of power system first a robust wide area damping controller(WRDC) with multiple outputs connected to multiple actuators is designed. The group of actuators involved in damping of oscillations in wide area control act as a self independent unit for different operating conditions of nominal system as well as for system with actuator faults. The unit is even effective for damping of power oscillations even when one or more actuators goes off and the number of active actuators is reduced. Reconfigurable control is added to the design of WRDC where a reconfiguration component(RC) is embedded in the feedback path of the controller. RC is designed along the lines of fault hiding principle and is activated only on occurrence of actuator fault. On activation RC connects to remaining active actuators and together make-up for loss of control action due to actuator faults. RC redistributes control effort among the active actuators to meet system performance objectives. Hence no redundant actuator is required post actuator fault to transfer control to prevent system performance from deteriorating. The multiple actuators involved in WAC of power system under reconfigurable control acts as one self contained unit capable to keep system response unaffected from any actuator faults. With fault hiding principle based reconfigurable control the RC acts as virtual actuator on occurrence of actuator fault. Under the proposed fault tolerant control design nominal wide area damping controller(WRDC) can be used without any changes to its parameter. The design of reconfiguration component that leads to self contained actuators unit is discussed below.

The schematic diagram illustrating working of reconfigurable control for fault tolerant WAC involving multiple actuators is shown in Fig. 2. \( A_1, A_2, \ldots, A_n \) are the \( n \) number of wide area control actuators connected to \( n \) outputs of wide area controller. The reconfigurable control on actuator fault introduces a new dynamical block called reconfiguration component(RC) in the feedback loop. The design of RC is along the lines of fault hiding principle(fhp). On activation of RC the input to controller(WRDC) in the Fig. 2 is the reconfigured system output \( (y_c) \) and output from controller is the new reconfigured signal\((u_c)\). While the actual input and output signals of power system on account of actuator fault are
A new state vector \( \mathbf{e} \) giving deviation in state trajectory of faulty system from nominal system is introduced. Where \( \mathbf{e} = x_f + \hat{x} \) modifies the state variable model as given in (15). The new state vector \( \mathbf{e} \), can be interpreted as the state of nominal system.

\[
\begin{pmatrix}
\dot{\mathbf{e}} \\
\dot{\hat{x}}
\end{pmatrix} =
\begin{pmatrix}
A & 0 \\
0 & A - B_i M_i
\end{pmatrix}
\begin{pmatrix}
\mathbf{e} \\
\hat{x}
\end{pmatrix}
+ 
\begin{pmatrix}
B \\
B - B_i N_i
\end{pmatrix} \mathbf{u}_c \tag{15}
\]

\[
y_c = \begin{pmatrix}
C \\
O
\end{pmatrix} \begin{pmatrix}
\mathbf{e} \\
\hat{x}
\end{pmatrix} \tag{16}
\]

The reconfigured signals \( \mathbf{u}_c \) and \( y_c \) in (15) are the output and input signals of controller(WRDC). As seen from (15) the reconfigured system dynamics(\( \mathbf{e} \)) presented to WRDC(\( \mathbf{u}_c \) and \( y_c \)) is such that no actuator fault has taken place. Inserting RC between WRDC and power system hides actuator fault from WRDC.

The parameters of RC are dependent on actuator fault. The relationship between the parameters(\( M_i, N_i \)) of RC and active actuators remaining in the wide area unit of actuators(\( \{A_1, A_2, ..., A_N\} \)) on any \( i^{th} \) actuator fault is given by (17). The \( i^{th} \) actuator fault is represented by input matrix \( B_i \) (with all zeros \( i^{th} \) column).

\[
(B_i, M_i, N_i) = \begin{cases}
(B_{01xn}, l_{0xn}) : \text{All – actuators – active} \\
(B_{0i, M_1, N_1}) : \{A_2, A_3, ..., A_N\}_{\text{Active}} \\
(B_{02, M_2, N_2}) : \{A_1, A_3, ..., A_N\}_{\text{Active}} \\
... \\
(B_{0N, M_N, N_N}) : \{A_1, A_2, ..., A_{N-1}\}_{\text{Active}}
\end{cases} \tag{17}
\]

This results in parameters of RC becoming dynamic with respect to actuator fault and change with respect to change in actuator fault as given in (17). For each actuator fault RC assumes related parameters from (17) and drives remaining active actuators to stabilize the system output. The control effort is redistributed by RC among active actuators to keep system response unaffected by actuator fault. More details on state variable model of reconfigured system and design of reconfiguration components can be found in [27, 28] and [29].

5 Numerical Results And Discussion

5.1 Case Study

One of the bench mark model for study of stability methods in power system, Kundur’s 2-Area Power System [20], is used here in testing and demonstrating efficacy of proposed method. [20] is used in several methods as in [6, 15] to demonstrate respective robust controllers in damping of low frequency power oscillations in power system. [20] comprises of 4 generating machines, set of tie lines connecting two areas Area-1 and Area-2. In the modified model a HVDC line is introduced between the two areas Area-1 and Area-2 for transmission of power between the regions. The line diagram of two area power system is shown in Fig. 3. A Static VAR compensator
(SVC) is configured in power system and installed at bus in the centre of tie-lines. The system parameters and related details are mentioned in [20, 30]. Each generator is represented by a sub-transient model and is of 5th order with two damper windings and rated at 1000 MVA. A IEEE type-1A D.C excitation system (3rd order), TG model (3rd order), Power system stabilizer (PSS) (3rd order) at generator input for damping of local modes. SVC rated at 200 MVA (2nd order), HVDC line transporting power at 510 kV (1st order).

5.2 Modal Analysis

The operating point considered is for an inter-area power transfer of 300 MW from Area-1 to Area-2. The small signal model of the power system at the nominal operating point is of order 65, obtained using Matlab toolbox PST [31]. In absence of WRDC system model is treated as open loop system in context of wide area control (WAC). The two critical eigen modes with insufficient damping are listed in Table 1.

Mode $l_1$ in Table 1 is inter-area mode where machines $G_1, G_2$ from Area-1 oscillates against $G_3, G_4$ from Area-2 [32]. Mode $l_2$ in Table 1 is an intra-area mode where machines from same area oscillate against each other. A wide area control scheme utilizing relevant system output as feedback signals ($y$) connected to WRDC and output from WRDC connected to suitable inputs of power system as wide area control signal($u$) is implemented. Machines $G_1, G_2$, HVDC system and SVC are selected as inputs for control signal($u$) coming from wide area controller. While signals $p_{e3}$ and $p_{e4}$ giving power generation at machines $G_3$ and $G_4$ are selected as feedback signals($y$) and connected to controller thereby completing closed loop system in context of wide area control. The method of residues is used in selecting $p_{e3}$ & $p_{e4}$ as output feedback signals of power system connecting it to WRDC [33]. Residue values are considered as index of observability and controllability of the modes of oscillations [34, 35]. The highest controllability of modes $l_1$ and $l_2$ is with WRDC connected to machine $G_2$.

Rotor speed ($\omega_3$) of generator ($G_3$) is chosen as performance signal. The eigen vectors corresponding to modes ($l_1$ and $l_2$) has $\omega_3$ as their largest component. This gives high observability of modes $l_1$ and $l_2$ in rotor speed $\omega_3$. The actuator and sensor placements in WAC of power system (G) is as given in Table 2. The output of WRDC ($u$) is fed to supplementary damping control inputs of (i) excitation system of $G_1$ (ii) excitation system of $G_2$ (iii) HVDC system & (iv) SVC. A detailed scheme of implementation of WAC in two area power system model is shown in Fig. 3. Where dash-lines represent wide area control signal($u$) to four selected actuators, and dotted lines represent system output feedback signal($y$) as input to WRDC.

5.3 Realization of WRDC: Nominal System Condition

The connection of WRDC and power system is as shown by the inter-connection between controller(K) and system(G) shown in Fig. 1. This requires WRDC controller of same order as of power system model. A bulky model of WRDC is practically not viable hence power system model is reduced from it’s original order(65th) to 8th order. Balanced model order reduction techniques are used to preserve the frequency response of the original system into reduced order system model [36]. As per the design criterion laid down for wide area controller(WRDC), in Section 3, minimum damping specified for closed loop power system(PS with WRDC) is $\xi_{min} = 0.1$. WRDC with four outputs is tested to meet the multiple design objectives from control effort optimization, disturbance attenuation to ensuring minimum damping specified in system. The four actuators selected for connecting to multiple output WRDC are in the following order (i) $G_1$ as actuator for single output controller, (ii) $G_1$, $G_2$ as actuators for two output WRDC, (iii) $G_1$, $G_2$ and SVC for WRDC with three outputs, to (iv) $G_1$, $G_2$, SVC and HVDC system for four output WRDC. The location of multiple

| Mode type | Damp($\zeta$) | Freq(Hz) |
|-----------|--------------|----------|
| Inter-area($l_1$) | 0.030 | 0.65 |
| Intra-Area($l_2$) | 0.046 | 0.97 |

| Table 2 Actuator and sensor locations |
|--------------------------------------|
| $i$ | $A_i$ | $S_j$ |
| 1 | $G_1$ | $P_{e3}$ |
| 2 | $G_2$ | $P_{e4}$ |
| 3 | HVDC | — |
| 4 | SVC | — |
actuators and feedback signals used in tuning of WRDC are listed in Table 2 & shown in Fig. 3.

Plot of eigen modes involving damping($\zeta$) vs frequency(f) for WRDC with single, two, three and four outputs is given in Fig. 4. It can be seen from Fig. 4 system damping is highest corresponding to WRDC with four outputs. Table 3 gives critical mode($\zeta_{min}$ and freq.) of closed loop system with WRDC having single output, two outputs, three outputs and four outputs. Figure 4 shows damping in system increases with increase in number of outputs of wide area controller. The damping achieved in system is largest in case of WRDC with four outputs($\zeta_{min} = 0.22$) double of specified damping($\zeta_{spe} = 0.1$) in design objective. This establishes effectiveness of having multiple output controller over single output controller. The state space model of WRDC($A_c, B_c&C_c$) is given in Appendix A.

In Fig. 5 closed loop power system with WRDC in feedback(four output controller) is compared against open loop system, for different operating conditions in terms of the chosen dynamic response($y_x$) i.e change in speed of generator $G_3(\Delta \omega)$. The different operating points considered vary from system under single tie line(on outage of other tie-line) to change in power flow across tie-lines for change in loads in the two area power system model. For every operating point considered closed loop(CL) system response under WRDC shows improved damping of oscillations compared to open loop(OL) system response.

### 5.4 Actuator Fault(s)

This part of the section demonstrates working of self contained actuators unit in restoring system performance in event of actuator faults taking place in wide area control of power system. The reconfigurable control on actuator fault restructures feedback loop such that WAC driven by multiple actuators makes for an self contained actuators unit capable of restoring system performance without depending on any redundant actuator outside the unit. The reconfiguration component(RC) embedded in the feedback loop gets activated on actuator fault and redistributes the wide area control input from WRDC among the remaining active actuators of the unit. The design implementation of reconfigurable control shows online-activation of reconfiguration component(RC) on actuator fault. This results in two reconfigured signals($y_c & u_c$) at input and output of WRDC, hiding actuator fault from it. In design implementation along with reconfigured signals shown are actual output and input signals of power system ($y_f & u_f$) respectively. The redistribution of control signal by RC on actuator fault to remaining active actuators is seen in actual input signal($u_f$). The distribution of control input among the actuators unit is dynamic and changes based upon actuator faults. The parameters of RC corresponding to a actuator fault are determined online and control reconfiguration happens in real time.
This makes for an autonomous fault tolerant control system and nominal controller (WRDC) along with RC makes for an fault tolerant wide area damping controller.

A disturbance is created in power system by outage of one of the two tie-lines for 1ms and system response ($\Delta$) i.e change in speed of generator $G_3$ is studied. A fault on actuator $A_1(G_1)$ is simulated at $t = 4s$. The online control reconfiguration caused by activation of RC together with remaining active actuators $\{A_2, A_3, A_4\}$ result in reconfigured signals $u_c$ and $y_c$ at output and input of nominal controller as shown in Fig. 6. The Fig. 6a shows actual input signal $u_f$ to the system, where input line corresponding to actuator $A_1$ (in color blue) goes to zero for $t \geq 4s$ indicating actuator fault. This causes activation of RC in system resulting in reconfiguration of system dynamics. The redistribution of control signals at $t=4s$ to remaining active actuators $A_2, A_3$ and $A_4$ can be clearly seen in signal $u_f$. In Fig. 6b the reconfigured control signal $u_c$ as seen by controller WRDC at system input is shown. In $u_c$, WRDC sees all actuators up and active for all the time, no redistribution of control signals and hence sees no actuator fault. The signal $y_f$ shown in Fig. 6c is actual output signal of power system that goes as feedback to WRDC. The effect of integration of RC at $t = 4s$ causing sudden reconfiguration of system dynamics can be seen in form of spike at $t = 4s$ in actual feedback signal $y_f$. Whereas the feedback signal reaching to WRDC is reconfigured signal $y_c$ (output of RC + $y_f$) shown in Fig. 6d. In $y_c$ WRDC sees no such disturbance at it’s input due to any actuator fault. The reconfigured
signals $y_c$ and $u_c$ thus successfully hides the fault at actuator $A_1$ from the WRDC, based on fault hiding principle. It aids in fast stabilizing the system response which otherwise is affected on actuator fault as shown in Fig. 8. The interfacing signals connecting WRDC to the reconfigured power system are $y_c$ & $u_c$. The parameter $M_1$ of RC to some arbitrary closed loop poles of reconfigurable block, on actuator fault at $A_1$ and corresponding to remaining active actuators $A_2, A_3, A_4$ is given in Appendix B.

The Fig. 7 shows system reconfiguration on actuator fault at $A_3$ at $t=4s$ and control action completed with remaining active actuators $\{A_1, A_2, A_4\}$ from the unit of wide area actuators. The reconfigured signals ($y_c$ and $u_c$) generated on fault at $A_3$, to actual input-output signals of system($y_{in} and u_{in}$) are shown in Fig. 7. The change in control signal($u_{in}$) at $t=4s$, caused by activation of RC and redistribution among the remaining active actuators can be seen in Fig.7a. The reconfiguration of system dynamics on account of activation of RC at $t=4s$ and its effect on output feedback signal $y_f$ is seen in Fig. 7c. While the two reconfigured signals($y_c$ and $u_c$) connecting WRDC to reconfigured system hides actuator fault at $A_3$ from it. The parameter $M_3$ of RC to some arbitrary closed loop poles of reconfigurable block, on actuator fault at $A_3$ and corresponding to active actuators set $\{A_1, A_2, A_4\}$ is given in Appendix B.

Similarly faults at other actuators could be simulated and signals generated by system reconfiguration could be discussed. The reconfigurable control causes change in system dynamics by inserting new dynamical block(RC) between WRDC and power system. RC on activation causes reconfiguration of system dynamics allowing for stabilizing system response affected from actuator fault. The effects of actuator faults on chosen system performance path($y_f$ i.e rotor speed of generator $G_3$) are shown in Figs. 8 and 9. In Fig. 8a shows wide area control input to power system on actuator fault at $A_1$ at $t=4s$. The input line corresponding to actuator $A_1$ becomes zero for $t \geq 4s$. It can be seen from Fig. 8a that in absence of RC there is no redistribution of control input among other active actuators of the unit. The Fig. 8b compares effect
of actuator fault at $A_3$ on system performance path $y_z$ with and without RC. In both the figures Figs. 8 and 9 it can be seen system response($y_z$) stabilizes fast in presence of RC compared to system response without RC. The actuators($A_1, A_2, A_3, A_4$) selected for wide area control action and tuned under reconfigurable control(following fault hiding principle), stabilizes system response in presence of actuator faults, without any need of redundant actuators thereby making for an self contained actuators unit.

Comparison of results from proposed method with other fault tolerant control methods on actuator and sensor faults in wide area control of power system is given in Table 4.

The results discussed from Figs. 6 and 7 clearly establishes group of actuators in WAC as self contained actuators unit not depending on any redundant actuators outside the unit, in case of actuator faults. While in [15] actuator fault severs feedback loop in WAC and requires control signal to be re-routed to redundant actuator. The use of multiple actuators in system as proposed here leads to higher damping compared to other two methods. Reconfigurable control (as proposed here) is activated only on occurrence of actuator fault unlike in [16] where designed controller is active even for nominal system condition and leads to conservative controller action in absence of fault.

6 Conclusion
A novel concept of self contained actuators unit in wide area control of damping in power system for nominal system condition under different operating points as well as for system affected by actuator faults is presented in the paper. A wide area robust damping controller is designed to meet multiple objectives from disturbance attenuation to ensuring minimum damping in system. Infinity norm minimization of closed loop transfer function and pole placement criterion is used in the design of wide area robust damping controller. The use of multiple output wide area controller feeding multiple actuators in power system allows for higher damping and fast settling of power oscillations in system. The wide area damping controller is tested for different operating conditions and controller is found suitable in providing sufficient damping in system compared to open loop system. The reconfigurable control design following fault hiding principle that is added to wide area controller is found to maintain sufficient system damping on actuator faults.

### Table 4: Comparison of results with other FTC methods in wide area control and damping of PS

| Paper        | Fault      | No. of active WAC actuators/sensors | Minimum Damping $\zeta_{\text{min}}$ | Dependent on redundant actuators/sensors | Switching of RC |
|--------------|------------|------------------------------------|-------------------------------------|------------------------------------------|-----------------|
| Proposed     | Actuator   | Dynamic Reconfigurable Control     | $\zeta_{\text{min}} > \zeta_{\text{spc}}$ | No (Self Contained Unit)                 | Automatic       |
| Raoufat M.E. [15] | Actuator | Static Reconfigurable Control | $\zeta_{\text{min}} = \zeta_{\text{spc}}$ | Yes                                     | Manual          |
| Sevilla [16] | Sensor     | Semi-Active                         | $\zeta_{\text{min}} = \zeta_{\text{spc}}$ | No                                      | Minimum Switching |
taking place in system. The reconfiguration component is activated on actuator fault and together with remaining active actuators from the same group (earlier to actuator fault) stabilizes system response. The group of actuators involved in wide area control and damping act as an self sufficient actuators unit for maintaining system damping and preserving system response even in the case of actuator faults. The reconfiguration component is dynamic and assumes parameters that change with respect to change in actuator fault but together with remaining active actuators act to maintain sufficient damping in system with or without actuator fault, under different operating points and independent of use of any redundant actuators.

Appendix A

$$A_c = \begin{bmatrix} 0.1710 & -1.7409 & 3.2733 & 1.6910 & 0.3461 & -4.8994 & -1.1374 & 7.2250 \\ 1.2781 & -1.3612 & 1.5381 & 0.9017 & -0.0372 & -4.5000 & -0.5359 & 4.4366 \\ -1.7444 & -2.1782 & -3.6012 & -8.1806 & 0.7019 & 2.4687 & 2.0896 & -2.7564 \\ -0.0557 & 0.7671 & 3.7192 & -0.3617 & -3.2694 & -0.8735 & 2.1639 & -2.2471 \\ 0.0426 & -0.5731 & 0.7163 & 5.3078 & -2.9143 & 2.0177 & 7.1287 & -6.7036 \\ 1.1957 & -0.7803 & 0.0736 & 0.4511 & -1.7304 & -3.2593 & -3.5096 & 4.5430 \\ -0.0961 & -0.4992 & -0.0162 & -1.7072 & 0.4617 & 1.5889 & -12.8076 & 24.1110 \\ 0.3499 & 0.1309 & -1.1687 & -3.8928 & -0.4294 & 1.5194 & -14.3748 & 0.8720 \\ \end{bmatrix}$$

$$B_c = \begin{bmatrix} 0.2391 & -0.4516 & -0.0998 & -1.4142 & 0.3205 & -1.4287 & 0.9617 & -0.9756 \\ 0.1014 & -0.2836 & -0.2957 & 1.0624 & 0.3243 & -0.9794 & 0.2547 & 0.9253 \\ \end{bmatrix}^T$$

$$C = \begin{bmatrix} 0.3680 & 0.0522 & 0.1192 & -0.0410 & -0.5885 & 0.2524 & 0.7456 & 1.1445 \\ 0.0423 & -0.2422 & -0.7053 & -0.6360 & 0.1930 & 0.4405 & 0.0217 & -1.5247 \\ 0.2223 & 0.7219 & 0.4906 & 1.3335 & 0.3904 & 1.6906 & -1.1098 & -0.8775 \\ -0.0077 & -0.0924 & -0.0642 & -0.0827 & -0.1096 & -0.2085 & 0.3493 & -0.1137 \\ \end{bmatrix}$$

Appendix B

$$M_1 = 1.0 \times 10^5 \begin{bmatrix} -0.1107 & 0.1545 & -0.2626 & 0.3001 & 0.2109 & 0.3395 & 0.0258 & -0.3972 \\ 0.5808 & 0.1024 & 0.2879 & -1.6944 & -0.7673 & 1.2410 & -0.1535 & 1.6303 \\ -0.3682 & 0.1071 & -0.2590 & 0.7594 & 0.2735 & 0.6111 & 0.0556 & -0.7189 \\ 0.1977 & -0.4128 & 1.0539 & -0.1729 & 0.0898 & -0.5675 & -0.0218 & 0.7391 \\ 0.1720 & 0.6105 & -0.6944 & -0.0690 & 0.0047 & 0.2157 & 0.0663 & -0.6616 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -0.5829 & 2.1839 & -2.7574 & 0.4306 & -0.2983 & 1.4691 & 0.0267 & -1.7801 \\ \end{bmatrix}$$

$$M_2 = 1.0 \times 10^5 \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -0.1107 & 0.1545 & -0.2626 & 0.3001 & 0.2109 & 0.3395 & 0.0258 & -0.3972 \\ 0.5808 & 0.1024 & 0.2879 & -1.6944 & -0.7673 & 1.2410 & -0.1535 & 1.6303 \\ -0.3682 & 0.1071 & -0.2590 & 0.7594 & 0.2735 & 0.6111 & 0.0556 & -0.7189 \\ 0.1977 & -0.4128 & 1.0539 & -0.1729 & 0.0898 & -0.5675 & -0.0218 & 0.7391 \\ 0.1720 & 0.6105 & -0.6944 & -0.0690 & 0.0047 & 0.2157 & 0.0663 & -0.6616 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -0.5829 & 2.1839 & -2.7574 & 0.4306 & -0.2983 & 1.4691 & 0.0267 & -1.7801 \\ \end{bmatrix}$$

Nomenclature

- $\delta$: rotor angle
- $\omega_{\text{load}}$: rotor and synchronous speed
- $\psi_d, \psi_q$: d-axis and q-axis flux linkages
- $\psi_f, \psi_{kd}$: flux linkage to field coil and d-axis damper coil
- $\psi_{kq1}, \psi_{kq2}$: flux linkages to two q-axis damper coils
- $E_{sd}$: exciter output voltage
- $i_f, i_{kd}$: current in field coil and d-axis damper coil
- $i_{kd1}, i_{kd2}$: current in two q-axis damper coils
- $K_A$: AVR gain constant
- $K_s$: svc gain constant
- $P_{HVDC}$: Supplementary control input of HVDC link
- $V_{dc}$: HVDC link modified ordered power
- $T_A$: AVR time constant
- $T_{d1}, T_{d2}$: d-axis and q-axis open circuit transient time constants
- $T_{d1}, T_{d2}$: d-axis and q-axis subtransient time constants
- $T_{1A}, \ldots T_{5A}$: SVC time constants
- $V_{mod}$: supplementary control input of Exciter
- $V_{mod}$: supplementary control input of SVC
- $V_{pss}$: voltage output of PSS
- $V_{ref}$: voltage reference set at input
- $x_d, x_q, x_{d1}$: direct axis, quadrature axis and leakage reactance of generator
- $x_d', x_q'$: d-axis and q-axis transient reactance of generator
- $x_d'', x_q''$: d-axis and q-axis subtransient reactance of generator
- $x_{d1}, x_{q1}$: d-axis and q-axis mutual reactance of generator
- $B_{svc}$: net susceptibility contributed by SVC
- $H, D$: rotor Inertia and damping coefficient
- $X_{1svc}, X_{2svc}$: SVC state variables

Acknowledgments

Not applicable.

Authors’ contributions

First author DVN has studied the fault tolerant control methods in wide area control of power systems. DVN has formulated and implemented the control design of online fault tolerant control feature for wide area damping controller. MSMR has supervised and guided the work and under whom DV has done the above research work. Both authors read and approved the final manuscript.

Funding

No funding received from any agency.

Availability of data and materials

The Kunduri two-Area four generator power system model can be found in [20, 30]. In [30] bench mark models for analysis and control of small signal oscillatory dynamics in power system are given.

Competing interests

The authors declare that they have no competing interests.

Author details

1 Faculty of Science & Technology, IFHE HYDERABAD, Shankerpally Road, 501203 Hyderabad, India. 2 Dept. of EE, CMR College of Engineering & Technology, Medchal Road, 501401 Hyderabad, India.
Received: 31 July 2019 Accepted: 2 January 2020
Published online: 05 February 2020

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