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Gene Function Prediction with Gene Interaction Networks: A Context Graph Kernel Approach

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Abstract—Predicting gene functions is a challenge for biologists in the post-genomic era. Interactions among genes and their products compose networks that can be used to infer gene functions. Most previous studies adopt a linkage assumption, i.e., they assume that gene interactions indicate functional similarities between connected genes. In this study, we propose to use a gene’s context graph, i.e., the gene interaction network associated with the focal gene, to infer its functions. In a kernel-based machine learning framework, we design a context graph kernel (CGK) to capture the information in context graphs. Our experimental study on a testbed of p53-related genes demonstrates the advantage of using indirect gene interactions and shows the empirical superiority of the proposed approach over linkage-assumption-based methods, such as GAIN and diffusion kernels.

Index Terms—Classification, gene pathway, kernel-based method, system biology

I. INTRODUCTION

DEV ELOPMENTS in genome sequencing have led to the identification of a large number of genes. However, most of these genes’ functions remain poorly known or unknown [1]. Annotating genes’ functions has become a challenge for biologists in the post-genomic era. Various computational techniques have been proposed to assist biological experiments in uncovering unknown gene functions.

In the early stages of computational modeling, individual genes’ physical, chemical, and biological characteristics were the major features used for function prediction. Recent studies have used gene interaction information and obtained promising results [2]. However, in most of these studies gene interactions are considered to be indicators of functional similarities between connected genes, which restricts the power of prediction models. In addition, the topology of gene interaction networks has seen limited use.

In this paper, we propose to predict a gene’s functions according to its context graph, which is defined as the gene interaction network composed of the genes interacting directly and indirectly with the focal gene. We propose a context graph kernel in a kernel-based machine learning framework that uses both gene features and structural characteristics of the context graph to infer the focal gene’s functions.

The remainder of this paper is organized as follows. Section 2 reviews related studies on gene function prediction using gene interaction information. Section 3 introduces the proposed context graph kernel method. Section 4 describes our experiments and results. Section 5 summarizes our conclusions and future directions.

II. LITERATURE REVIEW

Gene functions can be predicted through annotating individual genes [3] or gene clusters [4]. At the individual gene level, gene features such as gene sequences [5], molecule structures [6], and gene co-expression patterns [7] have been used for annotation. Recent studies observed that gene interactions in biological pathways (including gene-gene interactions, gene-protein interactions, and protein-protein interactions) are also related to the functions of genes. The significant amount of gene interactions [8] found in previous research can become another important resource for gene function prediction.

We review previous interaction-based function prediction studies along three dimensions: assumptions, levels of interactions, and computational techniques.

A. Assumptions

Previous studies are typically built upon a linkage assumption or a context assumption. A linkage assumption considers gene interactions as an indicator of a functional similarity between connected genes. This assumption comes from the observations that immediate neighbor genes [9] and level-2 neighbor genes [10, 11] have a high probability of sharing functions. Based on this assumption, a focal gene’s functions can be adopted from the majority of its neighbor’s functions (Fig. 1a and Fig. 1b).

The context assumption focuses on the relationship between a focal gene’s functions and the pattern of its context, i.e., its direct/indirect neighbors’ functions, sequences, or other characteristics. As illustrated in Fig. 1c, gene g can be predicted to have a certain function based on the fact that it interacts with genes having function X and Y. However, it may not have function X or Y. For example, growth factor receptors (such as EGFR) usually bind to a growth factor (such as EGF) and activate certain proteins (e.g., SHC) and kinases (e.g., PI3K) in signaling pathways [12]. From a gene function prediction perspective, if a gene/gene product (such
as PDGFR) is observed to be involved in a similar context of biological processes (binding to growth factors and activating SHC) may thus be predicted to be a growth factor receptor [13]. However, if the linkage assumption is taken, one may predict the gene to be a growth factor due to its interactions with other growth factor genes, which leads to a false prediction. In previous research, Schlitt et al. have considered with other growth factor genes, which leads to a false prediction. In previous research, Schlitt et al. have considered using direct neighbors as the context and predicted similar functions for genes with similar neighbors [14].

**Fig. 1.** Using gene interactions in gene function prediction. a) A linkage assumption assumes connected genes have similar functions. b) Indirect neighbors may have lower probability of sharing similar functions. c) A context assumption assumes that a gene’s functions are correlated with the patterns of its context. d) When multiple levels of gene interactions are used, genes with similar context graphs may have similar functions.

### B. Levels of Interactions

In previous gene function prediction research using gene interactions, both direct interactions between neighbor genes and multiple levels of interactions between indirect neighbor genes have been considered. Early studies based on direct interactions used the “guilt by association” rule under the linkage assumption to infer a focal gene’s functions as the most frequent ones among its neighbors [15, 16].

Considering multiple levels of interactions is a natural extension. Under the linkage assumption, the indirect neighbors may have weaker influence on the focal gene’s function prediction (Fig. 1b). Features describing second-level neighbors have been explicitly extracted and used in gene function prediction [10, 11, 17]. Hishigaki et al. proposed searching multiple levels of neighbors for the most frequent functions to predict labels of the focal gene [18]. Furthermore, some studies extend the scope of neighbors to the entire gene interaction network to take advantage of the global topology of the network [8, 19, 20]. Multi-level interactions can also be considered under the context assumption, where the context graph extends beyond direct neighbors of the focal gene (Fig. 1d) to determine the focal gene’s functions.

### C. Computational Techniques

Computational techniques for gene function prediction can be categorized into heuristic approaches and machine learning approaches. Heuristic approaches usually predefine rules to make predictions. For example, after defining the label propagation rule, function labels can be propagated through direct interactions [15] or the entire interaction network [20] to genes with unknown functions. The predefined rules can also be used to design objective functions for optimization models. Based on the “guilt by association” rule, function prediction is formulated as minimizing inconsistent function assignments of connected genes in the network [8, 19, 21, 22]. Simulated annealing [19] and iterative local search methods [8, 21, 22] have been proposed to find solutions for such models.

Machine learning approaches build prediction models from training instances. In particular, kernel-based methods have been frequently used in gene function prediction, due to their ability to capture gene interaction network structures. Based on the context assumption, linear kernels [23] and graph overlap similarities [24] have been used to model focal genes’ contexts. Based on the linkage assumption, diffusion kernels have been used to model genes’ positional characteristics in gene networks [25, 26].

### D. Research Gaps

**Table I** summarizes previous studies that use gene interactions in gene function prediction. We identify the following research gaps in previous research:

- Most studies tackled the gene function prediction problem under a linkage assumption. The use of context assumption is limited.
- Although both direct interactions and multi-level interactions have been used under the linkage assumption, the context-based studies used only direct interactions. The effect of indirect interactions under the context assumption still remains to be investigated.
- Heuristic approaches have been the major technique adopted. Several machine-learning-based studies used

| Previous studies | Type | Descriptions |
|------------------|------|--------------|
| Mayer et al. 2000 [15] | L/D/H | Guilt by association (majority voting) |
| Schwikowski et al. 2000 [9] | L/D/H | Guilt by association |
| Hishigaki et al. 2001 [18] | L/M/H | Multi-level neighbor majority voting |
| Schlitt et al. 2003 [14] | C/D/H | Similarity of neighbors |
| Vazquez et al. 2003 [19] | L/M/H | Minimize un-matching gene pairs |
| Karaoz, U. et al. 2004 [8] | L/H | Minimize un-matching gene pairs |
| Lanckriet et al. 2004 (a) [23] | L/M/ML | Diffusion kernel (classification by gene positions in the network) |
| Lanckriet et al. 2004 (b) [23] | C/D/ML | Linear kernel |
| Tsuda et al. 2004 [26] | L/M/ML | Locally constraint diffusion kernel |
| Yamanishi et al. 2004 [25] | L/M/ML | Diffusion kernel |
| Nabieva et al. 2005 [20] | L/M/H | Label propagation |
| Massjouni et al. 2006 [21] | L/M/H | Minimize un-matching gene pairs |
| Chua et al. 2006 [10] | L/H | Weighted neighbor function label counting |
| Murali et al. 2006 [22] | L/M/H | Minimize un-matching gene pairs |
| Xu et al. 2006 [17] | B/M/ML | KNN with neighbor-related features |
| Chua et al. 2007[11] | L/M/H | Weighted neighbor function label counting |
| Li et al. 2007 [16] | L/D/H | Guilt by association |
| Zhao et al. 2008 [24] | C/D/H | Similarity of neighbors |

*The three symbols separated by slashes represent the assumption, level of interactions, and computational technique respectively. The symbols’ meanings: L – linkage assumption; C – context assumption; B – both linkage assumption and context assumption; D – direct interactions; M – multi-level interactions; H – heuristic approach; ML – machine learning approach.*

Table I summarizes previous studies that use gene interactions in gene function prediction. We identify the following research gaps in previous research:
features of individual genes [5-7] without considering gene interactions. However, less attention has been paid to leveraging graph structures in statistical learning for gene function prediction.

III. RESEARCH DESIGN

To bridge the aforementioned research gaps, our study aims at predicting a gene’s functions based on its context in a gene interaction network. We also inspect the effect of using multiple levels of (indirect) interactions in function prediction. We choose a kernel-based machine learning approach in this research due to its documented good performance and ability to handle structural data [27].

A. A Kernel-based Approach

We formulate gene function prediction as a classification problem, i.e., categorizing genes into classes of gene functions. We first extract biological interactions from public databases to build interaction networks. In this research, we study only gene-gene interactions. For the databases of interactions between proteins or other gene products, we map all gene products to genes and create links between genes if their products interact. We then consolidate duplicates of these links to create gene-level interaction networks. While our proposed framework can also be applied to infer the functions of proteins in protein-protein interactions, we leave that to future research. We annotate genes with their known function labels. The genes with known functions are used as training instances to build classification models. Specifically, we build a binary classifier for each function label to test whether a gene has this function. Predictions on the testing instances by the classifiers can be validated against existing knowledge by domain experts or through further experiments.

In a kernel-based machine learning framework, we need to specify a kernel function and a kernel machine. The kernel function defines a similarity measure between data instances (i.e., genes in our research), while the kernel machine is in charge of building the model to classify the data instances. The performance of kernel-based methods is highly dependent on the design of kernel functions [28]. Thus, the main focus and contribution of the paper are to design a kernel function that can better capture structural patterns in gene interaction networks for the gene function prediction task. For the kernel machine, we choose the Support Vector Machines (SVM) [29] algorithm due to its competitive performance [30, 31].

B. A Context Graph Kernel

Recognizing the limitations of previous research, we adopt a context assumption and use multiple levels of gene interactions for gene function prediction. As shown in Fig. 1d, we represent each gene’s context as a graph. A context graph centers on the focal gene and includes its direct and indirect neighbors. According to the context assumption, genes with similar context graphs may share similar functions. Therefore we design a context graph kernel (CGK) to compute the similarity between context graphs.

Various graph kernels have been developed in previous data mining studies. For example, graph kernels were used to classify proteins based on the similarity of their molecular structures [6, 32, 33]. These graph kernels belong to the family of convolution kernels [34] and compute the graph similarity by accumulating the similarity scores of random walk paths on the graphs in a pair-wise manner.

Our proposed CGK also relies on the comparisons of random walk paths in the graphs. However, unlike traditional graph kernels that utilize all random walk paths in the graph, CGK considers only the random walk paths that start from the focal gene. This design is due to our objective of predicting the focal gene’s functions. Fig. 2 shows the context graph of gene $g_0$ and random walk paths starting from this focal gene. These paths represent the gene pathways related to the focal gene and thus may potentially indicate its functions. We calculate the similarity between two context graphs as the sum of pair-wise similarities of these random walk paths. Each path’s contribution is weighted according to its probability of traversal. Since longer random walk paths have a lower probability of being traversed, the genes that are far from the focal gene have less impact on the focal gene’s function.

The following procedure summarizes our kernel design:

(I) In the gene interaction network $G$ of a genome with $n$ genes $\{g_1, g_2, ..., g_n\}$, we represent gene $g_i$’s context graph as $G_i$. All random walks in $G_i$ start at $g_i$. At each gene (node) $g_i$, a random walk has a probability of $p_i(g_i)$ to stop and a probability of $p_i(g_i|g_j)$ to jump to one of $g_i$’s neighbors, $g_j$. Thus, a random walk path of length $l$, $h=(g_{<d,0>} \rightarrow g_{<d,1>} \rightarrow \ldots \rightarrow g_{<d,l>})$, has the probability of traversal:

$$P(h | G_i) = p_i(g_{<d,1>} | g_{<d,0>})p_i(g_{<d,2>} | g_{<d,1>}) \cdots \cdot p_i(g_{<d,l>} | g_{<d,l-1>})p_i(g_i),$$

(1)

where $g_{<d,>}$ indicates the $i$-th gene on the path $h$.

(II) After enumerating all random walk paths, the similarity between two context graphs, $K(G_i, G_j)$ is defined as the sum of the similarity scores of random walk paths weighted by the paths’ probability of traversal:

$$K(G_i, G_j) = \sum_{h_i \in H(G_i)} \sum_{h_j \in H(G_j)} K_{h}(h_i, h_j)P(h_i | G_i)P(h_j | G_j),$$

(2)

where $K_{h}(h_i, h_j)$ is the similarity score between two random walk paths $h_i$ and $h_j$, and $H(G_i)$ and $H(G_j)$ denote the sets of random walk paths in the two context graphs.

(III) The similarity between random walk paths is computed by multiplying the similarity of the corresponding nodes along the two paths. We define $K_{h}(h_i, h_j)$ as:

![Fig. 2. Random walk paths on a context graph](image-url)
where $|h_i|$ and $|h_j|$ are the lengths of the two paths $h_i$ and $h_j$, and $K'_{g}(g_{ch,k}, g_{ch,k})$ is a similarity function on nodes.

(V) In practice, the CGK kernel can be normalized for better classification performance.

$$K'(G_i, G_j) = K(G_i, G_j) / \sqrt{K(G_i, G_i)K(G_j, G_j)}$$

C. Computing the Context Graph Kernel in a Matrix Form

To compute the CGK by enumerating all random walk paths is computationally expensive. We introduce the computing the CGK based on the matrix form of the kernel.

In the gene interaction network $G$ of a genome with $n$ genes $\{g_1, g_2, ..., g_n\}$, we use two $n \times n$ matrices $M=\{M_{ij}\}=\{p(g_j|g_i)\}$ and $Q=\{Q_{ij}\}=\{p(g_i)\}$ to encode each node’s transition probability and stopping probability in the graph, respectively. The context graph kernel matrix of the entire genome $\tilde{K} = \{\tilde{K}_{ij}\} = \{K(G_i, G_j)\}$ can be represented as the summation of a series of matrices (Proposition 1 in Appendix):

$$\tilde{K} = \sum_{i=1,2,\ldots,\infty} K_i$$

where $K_i = (M^*Q)K_0(M^*Q)^{i}$, $K_{i+1} = M(K_0^iK_0)M^T$ ($i=1,2,\ldots,\infty$), and $K_0 = \{K_0(g_i, g_j)\}$ is the kernel matrix of node information. The operation $*$ is the Hadamard product (i.e., entrywise product) where $A*B = (a_{ij}b_{ij})$.

Each matrix $K_i$ covers the random walk paths of length $= i$ in the context graphs. It can be proved that $K_i + K_{i+1} + \ldots + K_r$ converges when $r$ approaches $\infty$ if the stopping probability is uniform or larger than 0.5 on all nodes (Proposition 2 in Appendix). Therefore, given a maximum length of random walk paths, $r$, we can use $K_i + K_{i+1} + \ldots + K_r$ to approximate the kernel $\tilde{K}$. With the decomposed form of $K_r$, the kernel $\tilde{K}$ can be computed by matrix operations with a time complexity in $O(n^2)$, where $n$ is the number of nodes in the network.

The matrix formulation also facilitates the investigation of the effect of indirect interactions on gene function prediction. Since all random walks start from the focal genes, each $K_i$ covers the genes that are $i$ step(s) away from the focal gene. While $\sum K_i$ will converge as $r$ increases, specifying a different $r$ restricts the CGK to a limited number of indirect interactions and may yield a different prediction performance. This may help us understand the effect of indirect interactions in gene function prediction.

IV. EXPERIMENTAL STUDY

A. Dataset

1) Human Genome Gene Interaction Network

In this study we use the collection of gene interactions from the BioGRID database [35] to construct a gene interaction network of human genomes. BioGRID is a free and well-known database with protein/gene interactions manually curated from Medline literature. We extract 38,225 relations related to Homo sapiens genes from BioGRID (version 2.026). By mapping proteins to genes and consolidating duplicate relations, we construct a gene interaction network with 19,623 non-directional relations among 7,167 genes.

2) Gene Function Labels

Following previous studies and domain experts’ suggestions, we use terms from Gene Ontology’s “biological process” hierarchy (downloaded in 2009) [36] as gene function labels. In GO, each term is associated with an evidence code indicating how the annotation to the term is supported (http://www.geneontology.org/GO.evidence.shtml). For the evaluation of gene function prediction methods, we used only the terms based on biological experimental evidences and computational analysis evidences and excluded the terms without solid evidence (i.e., NAS, IC, ND, IEA, and NR) in our experiments. After pre-processing, the “biological process” hierarchy has 8 second-level terms and 125 third-level terms (first level is “biological process”). We use the third-level terms as class labels in our study so as to have both enough classification granularity and sufficient training/testing data instances for each class. The genes whose functions are not documented are annotated as “unknown.”

3) A p53-related Testbed

The tumor suppressor gene, p53, plays a central role in the regulation of apoptosis and cell cycle arrest in cancer development. P53-related genes have attracted much attention and their functions are well-studied compared to other human genes. Therefore, we choose p53-related genes as our research testbed. In our previous research, we identified 2,045 p53-related genes from the Medline abstracts with a Natural Language Processing tool [37, 38]. After eliminating the genes without known functions, we obtain 1,566 genes within 35 third-level “biological process” functions. Nine of the classes with more than 50 instances are used in our experiments for evaluation. The dataset contains 819 genes in total. It should be noted that although the training/testing instances only include these p53-related genes, the gene interaction network-based approaches in our experiments take advantage of all (known) genes and gene interactions in the human genome to build gene function prediction models.

B. Evaluation Methodology

In the implementation of CGK, we specify a uniform stopping probability $p_r(g_j)=1-\lambda$ ($0<\lambda<1$) to generate random walks on the gene interaction network $G$. We also assume equal probability of jumping from one node to any of its neighbors, i.e., $p(g_j|g_i)=2/d(g_i)$, where $d(g_i)$ is the number of $g_i$’s interacting genes. After the calculation and normalization
of the CGK kernel, we use a popular SVM package, libSVM [39], to build classifiers.

We design the following two sets of experiments:

- **Experiment I** is to examine the effect of indirect interactions in gene function prediction. As described in 3.2.2, \( r \) controls the levels of indirect interactions that can be used in the kernel computation. In addition, the stopping probability \( p_i(g_i) = 1 - \lambda \) also controls the effect of indirect interactions in that longer random walks have smaller probabilities to be utilized in the kernel. Thus, we compare the performances of CGK using different \( r \) and \( \lambda \) settings in this experiment.

- **Experiment II** is to compare our proposed CGK-based method with other state-of-the-art methods, specifically four baseline methods from previous studies. In this experiment, we calculated the CGK kernel matrix till convergence (\( r=6 \) in our experiments).

To build a model with the CGK kernel, we need to specify the parameters of the SVM algorithm and \( \lambda \) (\( r \) does not need to be selected since one can calculate the kernel till converge). In the experiments, we use 50% of the data for parameter selection and the other 50% for performance testing. Through a 5-fold cross validation on the first 50% of data, we set \( \lambda \) to 0.9 (from 0.1 to 0.9), where the parameters for SVM are selected accordingly using the grid search tool provided by libSVM. With these parameters, the performance of the model on the second 50% of data is measured also using a 5-fold cross validation.

C. Evaluation Metrics

We evaluate the performance of the classification models using precision, recall, and F-measure, which are common evaluation metrics in gene function prediction studies [3, 8, 22]. Since one gene may have more than one function and one function may be associated with more than one gene, we calculate the three measures at both the instance level (i.e., gene level) and class level (i.e., function level). We also inspect instance-level performance with respect to the number of interacting genes to better understand the algorithms’ characteristics [18].

Instance-level precision \( P_i \), recall \( R_i \), and F-measure \( F_i \) are defined as:

\[
P_i = \frac{\text{correctly predicted functions of a gene}}{\text{all predicted functions of a gene}}
\]

\[
R_i = \frac{\text{correctly predicted functions of a gene}}{\text{all (known) functions of a gene}}
\]

\[
F_i = \frac{2 \times P_i \times R_i}{P_i + R_i}
\]

Class-level precision \( P_c \), recall \( R_c \), and F-measure \( F_c \) are defined as:

\[
P_c = \frac{\text{correctly predicted genes of a class}}{\text{all predicted genes of a class}}
\]

\[
R_c = \frac{\text{correctly predicted genes of a class}}{\text{all (known) genes of a class}}
\]

\[
F_c = \frac{2 \times P_c \times R_c}{P_c + R_c}
\]

D. Experimental Results and Discussion

1) **Experiment I: Effect of Indirect Interactions**

Experiment I examines the effect of indirect interactions for gene function prediction. Fig. 3 shows the instance-level and class-level performances using different values of \( r \) and \( \lambda \). When only direct interactions are considered (\( r=1 \)), the normalized CGK kernels are identical for different \( \lambda \)'s, which yield average F-measure scores of 25.5% at the instance level and 30.3% at the class level. When \( \lambda \) is larger than 0.5, taking into account of an additional level of indirect interactions (\( r=2 \)) leads to a significant increases in F-measure scores. When more levels of indirect interactions are included, the F-measure curves stabilize, which indicates the convergence of the kernel computation.

![Fig. 3. Performance of CGK using different levels of interactions](image)

It should be noted that a larger \( r \) indicates more indirect interactions used in our experiments. A larger \( \lambda \) indicates indirect interactions playing a more important role in the kernel. The experimental results demonstrate that incorporating information of indirect interactions may improve the gene function prediction performance. Our experiments suggest that computing CGKs for two or three levels (\( r = 2 \) or 3) gives a good approximation of the CGK, which can be considered in practical applications.

2) **Experiment II: CGK vs. Other Methods**

Based on the three dimensions in our literature review (i.e., assumption, interactions, and techniques), in Experiment II we compare our proposed context graph kernel method against four baseline methods from previous studies:

- **Linear kernel**: A linear kernel (LK) uses direct interactions under a context assumption [23]. For gene function prediction, the genes directly connected to the focal gene are used as features to represent the gene. The inner product of the feature vectors is used to calculate genes’ similarities. Genes with higher similarities, i.e., genes that share a larger number of neighbors, are predicted to have similar functions.

- **Diffusion kernel**: A diffusion kernel (DK) uses multi-level interactions under a linkage assumption. DK uses genes’ relative positions in the gene interaction network to predict their functions. Two genes that have more and shorter paths between them are more likely to be predicted to share the function labels [23, 25]. In addition to using the traditional diffusion kernel, we also adopt a locally constrained diffusion kernel (LDK) [26] due to its reported superior performance.
Gene Annotation using Interaction Network (GAIN): GAIN is a heuristic method using gene interaction networks under a linkage assumption, as reported in Karaoz et al. [8] and Murali et al. [22]. It optimizes gene function assignment by minimizing the inconsistency among connected genes in the network.

Neighborhood majority voting method (MV): Guided by the “guilt by association” rule [15], we construct a simple neighborhood majority voting classifier. The most dominant function label in the directly connected neighbors is predicted as the focal gene’s function.

In this research, the implementation of LDK and GAIN were provided by their authors, while the others were implemented by us.

Table II shows the instance-level prediction performances for different methods. Our proposed context graph kernel achieves the highest average precision, recall, and F-measure, which are significantly better than most other methods with a p-value < 0.05 in pair-wise t-tests. Its precision is not significantly different from GAIN (p-value ≈ 0.26). Compared to all learning-based methods, the context graph kernel outperforms by about 10% on all three measures. In these experiments, the majority voting algorithm has significantly worse performance than the other algorithms, which is consistent with previous research [19].

Table III shows the class-level performance of different classifiers. For most classes, the context graph kernel achieves the highest recall, while GAIN and the two diffusion kernels (DK and LDK) achieve the highest precision. All of these methods utilize the structure of the gene interaction network. Their performance differences show the different prediction power of the context assumption and the linkage assumption. In general, we observe a positive correlation between the class-level performance measures and the number of instances in the classes for CGK. For the classes with a larger number of instances, the F-measure of CGK is usually among the best. We identify that the classes “GO:42221 (response to chemical stimulus)” and “GO: 8283 (cell proliferation)” are difficult to classify (compared with classes with a similar number of instances) for most of the algorithms, while the class “GO:42330 (taxis)” has very high precision, recall, and F-measure when applying these algorithms. The differences in their performances indicate the different correlations between their functions and gene interactions, which are captured in this set of function prediction methods. Other types of information may need to be considered when the gene-interaction based algorithms do not perform well.

V. CONCLUSIONS AND FUTURE DIRECTIONS

In this research, we propose a context graph kernel for gene function prediction. This approach is based on a context assumption; it leverages multiple levels of interactions in gene interaction networks. Compared to other state-of-the-art methods that often use linkage assumptions and/or direct interactions, our proposed approach is highly competitive and achieves the highest F-measure. In addition, we find that our proposed approach works better on genes with a larger number

Fig. 4 shows different classifiers’ performances for genes with different numbers of interacting genes (or in graph theoretical terms, nodes with different degrees). The number of genes in each group is shown by column bars. In general, there is a positive correlation between classification performance and the number of interacting genes, except for

the majority voting algorithm and GAIN. Most algorithms were able to capture the information in a larger number of interactions for a more accurate prediction. Fig. 4 shows that the CGK performance is always among the best of all, which shows its ability of classifying different types of genes.
of interacting genes and classes with a larger number of genes.

The context graph kernel is capable of incorporating different types of node information in the gene function prediction task. In the future, we will extend the current research to include other types of biological data, such as gene sequence, molecular structure of gene products, and subcellular localization of gene products, as node information. We also plan to study the gene function prediction problem in multi-genome gene interaction networks.

**APPENDIX**

**Proposition 1:** In a genome’s gene interaction network \( G \) with \( n \) genes \( \{g_1, g_2, ..., g_n\} \), we represent the context graphs of gene \( g_1, g_2, ..., g_n \) as

\[
K(G_1, G_2) = \lim_{l \to \infty} \sum_{l=1}^{\infty} \sum_{h=1}^{n} \sum_{j=1}^{n} \left( \prod_{i=1}^{l} K_{g_1, g_2} \left( g_1, g_2 \right) \right) \cdot p_i(g_1, g_2) \cdot p_j(g_1, g_2).
\]

where \( K(G_1, G_2) \) is the kernel matrix of the entire genome; \( M = \{p_i(g_1)\} \) is the transition probability matrix; \( Q = \{p_j(g_2)\} \) is the stopping probability matrix; and \( K_0 = \{K_{g_1, g_2}\} \) is the node information kernel matrix. The context graph kernel matrix can be decomposed as:

\[
K_0 = \sum_{k} K_k\left( g_1, g_2 \right)
\]

(12)

where \( K_k = \{M^k Q K_0 M^k Q \} \), and \( * \) is the Hadamard product of matrices.

**Proof:**

Based on (3), random walk paths with different lengths do not affect the content graph kernel. Thus, we can group the random walk paths with the same length together and rewrite (2) as:

\[
K(G_1, G_2) = \sum_{l=1}^{\infty} \sum_{h=1}^{n} \sum_{j=1}^{n} \left( \prod_{i=1}^{l} K_{g_1, g_2} \left( g_1, g_2 \right) \right) \cdot p_i(g_1, g_2) \cdot p_j(g_1, g_2).
\]

Combining (11) into (13), the context graph kernel can be represented as:

\[
K(G_1, G_2) = \lim_{l \to \infty} \sum_{l=1}^{\infty} \sum_{h=1}^{n} \sum_{j=1}^{n} \left( \prod_{i=1}^{l} K_{g_1, g_2} \left( g_1, g_2 \right) \right) \cdot p_i(g_1, g_2) \cdot p_j(g_1, g_2).
\]

By converting the random walk paths in the pair-wise summation to node sequences and changing the order of summation and multiplication [33, 40], (14) is converted to:

\[
K(G_1, G_2) = \lim_{l \to \infty} \sum_{l=1}^{\infty} \sum_{k=1}^{n} \left( \prod_{i=1}^{l} K_{g_1, g_2} \left( g_1, g_2 \right) \right) \cdot p_i(g_1, g_2) \cdot p_j(g_1, g_2) \cdot K_{g_1, g_2} \left( g_1, g_2 \right).
\]

which can be represented as:

\[
K(G_1, G_2) = \lim_{l \to \infty} \sum_{l=1}^{\infty} K(G_1, G_2).
\]

(16)

We now work on proving that \( K(G_1, G_2) \) in (16) is the element of kernel matrix \( K_l \) in (12) using a mathematical induction method:

a) For \( l = 1 \)

Noticing that \( x = <h_i, 0> \) and \( y = <h_j, 0> \), from (15) we have:

\[
K(G_1, G_2) = K(G_{ch, bo}, G_{ch, bo})
\]

\[
= \sum_{x=1}^{n} \left( K_{g_1, g_2} \right) p_i(g_1, g_2) \left( g_1, g_2 \right) p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

According to the definition of \( K_l \):

\[
K_{l=1} = \sum_{x=1}^{n} \left( (M^* Q) K_0 (M^* Q) \right) p_i(g_1, g_2) \left( g_1, g_2 \right) p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

(17)

From the provided matrices in the proposition, we have:

\[
M^* Q = \{p_i(g_1) p_j(g_2)\}
\]

Since \( x = <h_i, 0> \) and \( y = <h_j, 0> \), and \( (M^* Q) \) from (15) we have:

\[
K_{l=1} = \sum_{x=1}^{n} \left( (M^* Q) K_0 (M^* Q) \right) p_i(g_1, g_2) \left( g_1, g_2 \right) p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

(18)

(19)

b) For \( l = 2 \):

From (15) we have:

\[
K(G_1, G_2) = \sum_{x=1}^{n} \left( K_{g_1, g_2} \left( g_1, g_2 \right) \right) \cdot p_i(g_1, g_2) \left( g_1, g_2 \right) \cdot p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

\[
= \sum_{x=1}^{n} \left( (M^* Q) K_0 (M^* Q) \right) p_i(g_1, g_2) \left( g_1, g_2 \right) p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

According to the definition of \( K_l \):

\[
K_{l=2} = \sum_{x=1}^{n} \left( (M^* Q) K_0 (M^* Q) \right) p_i(g_1, g_2) \left( g_1, g_2 \right) p_j(g_1, g_2) \left( g_1, g_2 \right).
\]

(20)

(21)
\[
\begin{align*}
&= \sum_{<k_1,k_2>,<j_1,j_2>}
\left( G_k(g_{ch,k_1},g_{ch,j_1})p_i(g_{ch,k_1} | g_{ch,j_1})
\cdot p_i(g_{ch,j_1} | g_{ch,j_2})K(G_{ch,k_1},G_{ch,j_2})\right) \\
& \quad \cdot p_i(g_{ch,j_2} | g_{ch,j_1})K(G_{ch,j_2},G_{ch,k_1})
\end{align*}
\]

(22)

According to (21) and (22), \( K_{i+1} = K_{i} + K_{i+1} \). Thus, any \( K_{G_1,G_1} \) in (16) is the element of kernel matrix \( K \) in (12), i.e., the context graph kernel can be decomposed to the forms in (12).

**Proposition 2:** For the context graph kernel, if node information \( K_i() \) is normalized and a) there is an uniform stopping probability \( p_i(g) \) or b) \( p_i(g) > 0.5 \), then the calculation of the kernel converges when more levels of interactions are included in the context graph, i.e., the process of \( K = K_1 + K_2 + K_3 + \ldots + K_i \) converges when \( i \) approaches \( \infty \).

**Proof:**

According to (6), we have:

\[
K(G_1,G_1) = K(G_1,G_1) + K(G_1,G_2) + K(G_1,G_3) + \ldots \text{, (23)}
\]

in which all similarity measures are non-negative numbers.

According to the rule of d'alambert (i.e., ratio test), such a non-negative series summation converges if

\[
\lim_{k \to \infty} \frac{K(G_1,G_1)}{K(G_1,G_k)} < 1.
\]

Base on (15), we can have:

\[
K(G_1,G_k) = \left[ \sum_{<k_1,k_2>,<j_1,j_2>}
G_k(g_{ch,k_1},g_{ch,j_1})p_i(g_{ch,k_1} | g_{ch,j_1})
\cdot p_i(g_{ch,j_1} | g_{ch,j_2})p_i(g_{ch,j_2} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})
\right]
\]

(24)

Since node information \( K_i() \) is normalized:

\[
K(G_1,G_k) \leq \left[ \sum_{<k_1,k_2>,<j_1,j_2>}
G_k(g_{ch,k_1},g_{ch,j_1})p_i(g_{ch,k_1} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})p_i(g_{ch,j_2} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})
\right]
\]

(25)

a) For the first condition, \( p_i(g) \) is uniform, thus:

\[
K(G_1,G_k) \leq \sum_{<k_1,k_2>,<j_1,j_2>}
G_k(g_{ch,k_1},g_{ch,j_1})p_i(g_{ch,k_1} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})p_i(g_{ch,j_2} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})
\]

(26)

b) For the second condition:

Since \( p_i(g) < 1 \), we can first relax (24) to:

\[
K(G_1,G_k) \leq \sum_{<k_1,k_2>,<j_1,j_2>}
G_k(g_{ch,k_1},g_{ch,j_1})p_i(g_{ch,k_1} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})p_i(g_{ch,j_2} | g_{ch,j_1})p_i(g_{ch,j_1} | g_{ch,j_2})
\]

(27)

Since \( p_i(g) > 0.5 \), this formula is obviously less or equal to 1. Thus, \( \lim_{k \to \infty} K(G_1,G_k) < 1 \), and the kernel converges when more levels of interactions are included.

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**REFERENCES**

[1] A. J. Enright, V. Kunin, and C. A. Ouzounis, "Protein families and TRIBES in genome sequence space," *Nucleic Acids Research*, vol. 31, pp. 4632-4638, AUG 1 2003.

[2] P. Z. Hu, G. Bader, D. A. Wigle, and A. Emili, "Computational prediction of cancer-gene function," *Nature Reviews Cancer*, vol. 7, pp. 23-34, JAN 2007.

[3] R. Sharan, I. Ulltsky, and R. Shamir, "Network-based prediction of protein function," *Molecular Systems Biology*, vol. 3, MAR 2007.

[4] M. A. Huynen, B. Snel, C. von Mering, and P. Bork, "Function prediction and protein networks," *Current Opinion in Cell Biology*, vol. 15, pp. 191-198, APR 2003.

[5] L. J. Jensen, R. Gupta, H. H. Staerfeldt, and S. Brunak, "Prediction of human protein function according to Gene Ontology categories," *Bioinformatics*, vol. 19, pp. 635-642, MAR 22 2003.

[6] K. M. Borgwardt, C. S. Ong, S. Schonauer, S. V. N. Vishwanathan, A. J. Smola, and H. P. Kriegel, "Protein function prediction via graph kernels," *Bioinformatics*, vol. 21, pp. 147-156, JUN 2005.

[7] P. Pavlidis, J. Weston, J. S. Cai, and W. S. Noble, "Learning gene functional classifications from multiple data types," *Journal of Computational Biology*, vol. 9, pp. 401-411, 2002.

[8] U. Kao, T. M. Murial, S. Letovsky, Y. Zheng, C. M. Ding, C. R. Cantor, et al., "Whole-genome annotation by using evidence integration in functional-linkage networks," *Proceedings of the National Academy of Sciences of the United States of America*, vol. 101, pp. 2888-2893, MAR 2 2004.

[9] B. Schwikowski, P. Uetz, and S. Fields, "A network of protein-protein interactions in yeast," *Nature Biotechnology*, vol. 18, pp. 1257-1261, DEC 2000.

[10] H. N. Chua, W. K. Sung, and L. Wong, "Exploiting indirect neighbours and topological weight to predict protein function from protein-protein interactions," *Bioinformatics*, vol. 22, pp. 1623-1630, JUL 1 2006.

[11] H. N. Chua, W. K. Sung, and L. Wong, "Using indirect protein interactions for the prediction of Gene Ontology functions," *BMC Bioinformatics*, vol. 8, 2007.

[12] C. J. Wu, Z. J. Chen, A. Ullrich, M. I. Greene, and D. M. O'Rourke, "Inhibition of EGFR-mediated phosphoinoside-3-OH kinase (PI3-K) signaling and glioblastoma phenotype by Signal-Regulatory Proteins (SIRPs)," *Oncogene*, vol. 19, pp. 3999-4010, AUG 17 2000.

[13] R. A. Klinghoffer, B. Duckworth, M. Valius, L. Cantley, and A. Kazlauskas, "Platelet-derived growth factor-dependent activation of phosphatidylinositol 3-kinase is regulated by receptor binding of SH2-domain-containing proteins which influence Ras activity," *Molecular and Cellular Biology*, vol. 16, pp. 5905-5914, OCT 1996.

[14] T. Schlitt, K. Palin, J. Rung, S. Dietmann, M. Lappe, E. Ukkonen, et al., "From gene networks to gene function," *Genome Research*, vol. 13, pp. 2568-2576, DEC 2003.
[15] M. L. Mayer and P. Hieter, "Protein networks - built by association," Nature Biotechnology, vol. 18, pp. 1242-1243, DEC 2000.

[16] Y. Tan and J. Wang, "A support vector machine with a hybrid kernel and minimal Vapnik-Chervonenkis dimension," IEEE Transactions on Neural Networks, vol. 16, pp. 385-395, APR 2004.

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[18] H. Hishigaki, K. Nakai, T. Ono, A. Tanigami, and T. Takagi, "Assessment of prediction accuracy of protein function from protein-protein interaction data," Yeast, vol. 18, pp. 523-531, APR 2001.

[19] A. Vazquez, A. Flammini, A. Maritan, and A. Vespignani, "Global protein function prediction from protein-protein interaction networks," Nature Biotechnology, vol. 21, pp. 697-700, JUN 2003.

[20] W. C. Ma, D. Yang, X. W. Wang, and M. Zhang, et al., "Finding finer functions for partially characterized proteins by protein-protein interaction networks," Chinese Science Bulletin, vol. 52, pp. 3363-3370, DEC 2007.

[21] K. Tsuda and W. S. Noble, "Learning kernels from biological networks," Bioinformatics, vol. 21, pp. 976-983, MAY 2005.

[22] H. Kashima, K. Tsuda, and A. Iokuchi, "Marginalized kernels between multiple genomic data," Bioinformatics, vol. 20, pp. 2626-2635, NOV 1 2004.

[23] D. Haussler, "Convolution kernels on discrete structures," UC Santa Cruz 1999.

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[27] M. L. Mayer and P. Hieter, "Protein networks - built by association," Nature Biotechnology, vol. 18, pp. 1242-1243, DEC 2000.

[28] H. Hishigaki, K. Nakai, T. Ono, A. Tanigami, and T. Takagi, "Assessment of prediction accuracy of protein function from protein-protein interaction data," Yeast, vol. 18, pp. 523-531, APR 2001.

[29] A. Vazquez, A. Flammini, A. Maritan, and A. Vespignani, "Global protein function prediction from protein-protein interaction networks," Nature Biotechnology, vol. 21, pp. 697-700, JUN 2003.

[30] W. C. Ma, D. Yang, X. W. Wang, and M. Zhang, et al., "Finding finer functions for partially characterized proteins by protein-protein interaction networks," Chinese Science Bulletin, vol. 52, pp. 3363-3370, DEC 2007.

[31] K. Tsuda and W. S. Noble, "Learning kernels from biological networks," Bioinformatics, vol. 21, pp. 976-983, MAY 2005.

[32] H. Kashima, K. Tsuda, and A. Iokuchi, "Marginalized kernels between multiple genomic data," Bioinformatics, vol. 20, pp. 2626-2635, NOV 1 2004.

[33] D. Haussler, "Convolution kernels on discrete structures," UC Santa Cruz 1999.

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[35] B. J. Breitkreutz, C. Stark, and M. Tyers, "The GRID: The General Repository for Interaction Datasets," Genome Biology, vol. 4, 2003.

[36] M. Ashburner, C. A. Ball, J. A. Blake, D. Botstein, H. Butler, J. M. Cherry, et al., "Gene Ontology: tool for the unification of biology," Nature Genetics, vol. 25, pp. 229-230, MAY 2000.

[37] X. Li, H. Chen, Z. Huang, H. Su, and J. D. Martinez, "Global mapping of gene/protein interactions in PubMed abstracts: A framework and an experiment with P53 interactions," J Biomed Inform, Jan 17 2007.

[38] D. M. McDonald, H. Chen, H. Su, and B. B. Marshall, "Extracting gene pathway relations using a hybrid grammar: the Arizona Relation Parser," Bioinformatics, vol. 20, pp. 3370-3378, 2004.

[39] C.-C. Chang and C.-J. Lin, "LIBSVM: a library for support vector machines," in http://www.csie.ntu.edu.tw/~cjlin/libsvm, 2001.

[40] H. Kashima, K. Tsuda, and A. Inokuchi, "Kernels for Graphs," in Kernel Methods in Computational Biology: MIT Press, 2004.