Estimation of intraband and interband relative coupling constants from temperature dependences of the order parameter for two-gap superconductors

S.A. Kuzmichev · T.E. Kuzmicheva · S.N. Tchesnokov · V.M. Pudalov · A.N. Vasiliev

Abstract

We present temperature dependences of the large and the small superconducting gaps measured directly by SnS-Andreev spectroscopy in various Fe-based superconductors and MgB$_2$. The experimental $\Delta_{L,S}(T)$ are well-fitted with a two-gap model based on Moskalenko and Suhl system of equations (supplemented with a BCS-integral renormalization). From the fitting procedure, we estimate the key attribute of superconducting state — relative electron-boson coupling constants and eigen BCS-ratios for both condensates. Our results evidence for a driving role of a strong intraband coupling in the bands with the large gap, whereas interband coupling is rather weak for all the superconductors under study.

Keywords

High-temperature superconductors · Two-gap superconductivity · Iron Pnictides · MgB$_2$ · Andreev spectroscopy · MARE spectroscopy

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1 Introduction

In spite of the intensive theoretical and experimental studies stimulated by the recent discovery of Fe-based superconductors in 2008 [1], many aspects of the multiband superconducting state are not fully understood yet. Particularly, one of the candidates for pairing in Fe-HTS is the spin-fluctuation-based pairing mechanism that leads to the $s^{\pm}$ symmetry of the order parameter [2]. A different mechanism, where pairing is mediated by orbital fluctuations [3], leads to the $s^{++}$ state. Among the iron-based superconductors, the 1111 family have the simplest band structure [4,5]. The bands crossing the Fermi level form quasi-two-dimensional sheets at the Fermi surface. According to recent ARPES studies, they can be considered as two effective electron and hole bands where the large (L) and the small (S) superconducting gaps are developed at $T < T_C$ [6]. However, despite the apparent simplicity, the majority of the experimental techniques face with serious troubles probing the values of the order parameter in 1111. The absence of single crystals of sufficient dimensions, and a charged surface of cryogenic clefts [7,8] strongly distort the experimental data. As a result, the values of superconducting gaps and corresponding BCS-ratios are very contradicive: for oxypnictides, $2\Delta_L/k_BT_C$ vary more than by a factor of 6 (for a review, see [9,10] and Refs. therein), from BCS-limit 3.5 up to 22 [11]. Temperature dependences of the gaps are also ambiguous (the data are reviewed in [10,12], see also Refs. therein). For example, in [13] a BCS-like temperature dependence was found for both gaps in SmO(F)FeAs, whereas in LaO(F)FeAs the large gap turned to zero at $T \approx 2/3T_C$ while the small gap was closed quite linearly and survived till the $T_C$. The latter was recognized as an artifact [13] and was reproduced nowhere in literature.

Fortunately, the 1111 oxypnictide superconductors are good candidates for probing by multiple Andreev reflections effect [14] spectroscopy. Here we present di-
rectly determined temperature dependences of the large and the small gaps in various 1111 compounds with the wide range of critical temperatures 21.5K ≤ TC ≤ 50K. The measured ΔL,s(T) dependences were fitted using a two-band BCS-like model with a renormalized BCS (RBCS) integral based on Moskalenko and Suhl system of gap equations [15,16,17]. The relative values of electron-boson coupling constants λi,j/λLL (i, j = L, S) are estimated. The data for 1111 oxypnictides are compared with Δ(T) and λi,j for LiFeAs and Mg1−xAlxB2.

2 Experimental details

We used LiFeAs single crystals with critical temperature TC,ulk ≈ 16–17K (the synthesis is detailed in [18]), and the following polycrystalline samples: fluorine-doped LaO1−xFeAs with TC,ulk ≈ 22–28K [19,20], and Sm1−xThxFeAs with a wide range of thorium doping and critical temperatures TC,ulk ≈ 25–55K [8,21], optimal oxygen-deficient GdO0.88FeAs with TC,ulk ≈ 50K [22], and Mg1−xAlxB2 with TC,ulk ≈ 21.5–40K [23,24]. The common feature of the samples under study is a layered crystal structure.

In our studies, superconducting gaps and Δ(T) temperature dependences were probed by Andreev spectroscopy of superconductor - normal metal - superconductor (SnS) contacts [13], and intrinsic multiple Andreev reflections effect (IMARE) spectroscopy [25,26]. SnS-contacts were formed by precise cleaving of the superconducting samples at T = 4.2K using a break-junction technique [27]. Under such cleavage, a layered sample exfoliates along the ab-planes; as a result, it contains two crenel clefts separated by a weak-link. For Fe-based superconductors of the 1111, and 111 families [12,20,23,24,30,31], the current-voltage characteristic (CVC) and the dynamic conductance correspond to a ballistic [32] high-transparent SnS-Andreev contact [33,34,35]. The break-junction technique enables the formation of clean crenetic clefts, true 4-probes connection, thus preventing overheating of the contact area, and easy mechanical readjustment. It is well-applicable for both single crystals and polycrystalline samples of layered material [28]. Our dV/dV measurements were performed directly by a modulation technique. We used a current source with ac frequency less than 1kHz. The results obtained with this setup are insensitive to the potential presence of parallel ohmic conduction paths; the latter, if present, only shift dynamic conductance curves along the vertical axis.

The multiple Andreev reflections effect occurring in ballistic SnS interface manifests itself as a pronounced excess current at low bias voltages (so-called foot area), and a series of dynamic conductance dips at certain positions Vn = 2Δ/en, where n is a natural subharmonic order; these features are called subharmonic gap structure (SGS). The gap value may be directly determined from the SGS positions over all the temperature range from 0 to TC with no dl(V)/dV fitting [33]. In case of two-gap superconductor, two such SGS’s should be observed. Along with multiple Andreev reflections effect in single SnS-contacts, in layered samples we observe an intrinsic multiple Andreev reflections effect (IMARE) in the stack structures of S-n-S-n-...-S-type [10,12,26,30,31]. The IMARE is similar to intrinsic Josephson effect [30], and was first observed in Bi cuprate superconductors [37]. Since the array of Andreev contacts represents a sequence of m identical SnS junctions, the SGS appears at Vn = m·2Δ/en bias voltages. We have shown that with m increasing, the contribution of parasitic effects decreases, facilitating observation of bulk superconducting gaps [20].

3 Results and discussion

Figure 1 shows normalized dynamic conductance curves for Andreev array (2 junctions in the stack) for LaO1−xFeAs sample. Note that the absolute dynamic conductance decreases with temperature, while the dl(V)/dV spectra in Fig. 1 are shown in arbitrary units, and offset vertically for clarity. The inset of Fig. 2 shows current-voltage characteristic (CVC) for this contact at T = 4.2K with a pronounced excess current at low biases (foot). The contact has a local critical temperature TC,ocal ≈ 22K corresponding to the contact area transition to the normal state; above this temperature the CVC becomes ohmic-like and free of an excess conductance. Taking the known product of quasiparticle mean free path and normal-state resistivity pl ≈ 10−10Ωcm² for 1111 compounds [20,28,39], we get l ≈ 50nm. Then, using Sharvin formula [32], and the resistance of this contact R ≈ 28Ω (here and below all calculations refer to a single junction in the array), we estimate the contact diameter a = 4/3π× pl/R ≈ 12nm ≪ l. The average crystallite dimensions are 60–70µm in Sm-1111 samples under study, and 10–40µm in La-1111 samples. These values are much larger than the estimated contact diameter a, thus providing local study of crystallites. Since a ≪ l, and the resistance of this contact decreases with temperature increasing, we conclude that our measurements are in the clean ballistic SnS-Andreev mode [40]. The same could be concluded for Mg1−xAlxB2 samples we used. The estimated pl range is (2–5) × 10−12cm², and l ≈ 80nm [41,42]. For our SnS-contacts, R = 1–22Ω, which leads to the estimate of the contact diameter a = 2–15nm. Obviously, a ≪ l, and less than the typical grain dimensions of about 100nm for MgB2 [24,28]. On an appearance
of any parallel ohmic contact, the dynamic conductance in a sample circuit increases, which could lead to underestimation of the Sharvin contact resistance. Since $a \sim 1/\sqrt{R}$ in a ballistic contact, true diameter of Andreev contact may be smaller than the above estimate.

At $T = 4.2 \, \text{K}$, dynamic conductance peculiarities located at $|V| \approx 10.8 \, \text{mV}$ and $|V| \approx 5.4 \, \text{mV}$ (marked in Fig. 1 as $n_S = 1$ and $n_S = 2$, respectively) correspond to the first and the second Andreev minima related with the large gap $\Delta_L \approx 5.4 \pm 0.5 \, \text{meV}$. Andreev peculiarities for the small gap $\Delta_S \approx 1.4 \pm 0.3 \, \text{meV}$ are marked with $n_S = 1$ labels and arrows. These values are close to those obtained by Andreev spectroscopy previously [20, 43]. Dips at $|V| \sim 1.4 \, \text{mV}$ related to the beginning of the foot area are sharp at $T = 4.2 \, \text{K}$ and then becoming smeared with temperature. With temperature increasing, the SGS peculiarities for both gaps move towards zero bias, and at $T_{C_{\text{local}}}^{\text{local}} \approx 22 \, \text{K}$ the $\text{d}I/\text{d}V$ curve becomes linear. Taking the position of SGS peculiarities for the large and the small gap, we directly obtain temperature dependences $\Delta_L,S(T)$ presented in Fig. 2 (by solid circles for $\Delta_L(T)$, and by open circles for $\Delta_S$). The temperature behaviour of the large and the small gap for LaO$_{1-x}$F$_x$FeAs looks like that for Sm$_{1-x}$Th$_x$OFeAs shown in Fig. 3, and for other Fe-based superconductors [10, 12, 29, 30, 31, 44, 45, 46].

A two-band BCS-like superconducting system is described by a matrix of four electron-boson coupling constants $\lambda_{ij} = V_{ij} N_j$, $i, j = L, S$ ($L$ index corresponds to the bands with the large gap, $S$ index —to the bands with the small gap), where $V_{ij}$ is the interaction matrix element between $i^{th}$ and $j^{th}$ bands, $N_j$ is the normal-state density of states at the Fermi level in $j^{th}$ band [15, 16]. Varying the relation between intraband and interband coupling, one may model various temperature dependences of the gaps. Obviously, in a case of zero interband interaction ($V_{LS} = V_{SL} = 0$), the large and the small gaps follow BCS-type curve and close each at its eigen critical temperature $T_{C,L,S}$ [17, 18]. By contrast, in Fe-based superconductors [10, 12, 29, 30, 31, 44, 45, 46] as well as in Mg$_{1-x}$Al$_x$B$_2$ [17, 49, 50] within the wide range of critical temperatures we observe the $\Delta_L,S(T)$ deviation from the single-gap BCS-like dependences: $\Delta_L(T)$ follows BCS type at the whole, but slightly bends down, whereas $\Delta_S(T)$ at first falls rapidly, then flattens, and finally turns to zero at $T_{C_{\text{local}}}^{\text{local}}$. As a result, the two gaps close at the common critical temperature $T_{C_{\text{local}}}^{\text{local}}$.

The temperature behaviour presented in Figs. 2, 3 is typical for two-band superconductor with a moderate interband interaction $17, 47$. Taking into account recent ARPES studies that revealed two effective bands in 1111-oxypnictides [6], we fit the obtained $\Delta_L(S)(T)$ by a two-band Moskalenko and Suhl gap equations [15, 16, 17] within RBCS model that allows a renormalization of $T_{C_{\text{local}}}^{\text{local}}$ to fit a realistic $2\Delta/k_BT_C$ BCS-ratio. The theoretical fitting curves (solid lines in Figs. 2, 3) agree well with the experimental data, thus showing the simple two-band RBCS model to be appropriate for 1111 superconductors. To fit $\Delta_L(S)(T)$ we used experimental values of $\Delta_L,S(4.2K)$, $T_{C_{\text{local}}}^{\text{local}}$, and three fitting parameters: $\alpha = \lambda_{LS}/\lambda_{SL}$, the relation between intra- and interband coupling rates $\beta = \sqrt{V_L/V_S}$, and the eigen critical temperature for the condensate with the small gap $T_{C_{\text{local}}}^{S}$. The only limitation for the latter parameter is evident: $2\Delta_S/k_BT_{C_{\text{local}}}^{S} > 3.52$. Red dashed lines correspond to the two-band BCS-like dependences estimated by us for $\Delta_S(T)$ and $\Delta_L(T)$ in a hypothetical case of zero interband coupling. Easy to note the condensate with the large gap looses about 14% of eigen $T_C$ value due to interband coupling. In comparison with $\Delta_L(T)$ dependence for 1111 compounds from Fig. 3, $\Delta_S(T)$ deviates weaker. By contrast, the bending of $\Delta_S(T)$ function is greater than $\Delta_S(T)$ for 1111, which points to weaker interband coupling rates in Mg$_{1-x}$Al$_x$B$_2$ system, probably due to the MgB$_2$ bands orthogonality in the $k$-space.
Temperature dependences of $\sigma$- and $\pi$-gaps in Al-doped Mg$_{1-x}$Al$_x$B$_2$ with $T_{C}^{local}$ ≈ 21.5 K are shown in Fig. 4 by solid and open triangles, respectively. The temperature influence on the corresponding dynamic conductance for this contact is presented in [49]. For clarity, we plot the normalized dependence $\Delta_x(T) / \Delta_x(0)$ by crossed triangles. Obviously, the $\sigma$- and $\pi$-gap behave differently with temperature increasing, thus the corresponding Andreev peculiarities in $\text{d}I(\text{V})/\text{d}V$-spectra relate to distinct superconducting condensates.

From the fitting procedure, we directly estimate some important parameters of the two-gap superconducting state in GdO$_{0.88}$FeAs, Sm$_{1-x}$Th$_x$OFeAs, LaO$_{1-x}$F$_x$FeAs, and Mg$_{1-x}$Al$_x$B$_2$, summarized in Table 1. The data on LiFeAs are presented for comparison; here and below the effective value of the large gap was taken from Ref. [31]. The gap temperature dependences for all superconductors under study demonstrate rather weak interband coupling. For oxypnictides, the eigen BCS-ratio (in a hypothetical case of zero interband coupling $V_{LS} = 0$) for the large gap remains nearly constant within the whole range of critical temperatures $T_C = 22–50$ K, and on the average, $2\Delta_L/k_BT_C^0 \approx 4.4$. This value exceeds the weak-coupling BCS-limit 3.52, thus corresponding to a strong intraband coupling in the bands with the large gap. Due to a nonzero interband interaction, the common critical temperature decreases by 20% for 1111 superconductors in comparison with the eigen $T_C^0$ for the “driving” bands with the large gap: in a hypothetical case of $V_{LS} = 0$, the critical temperature for oxypnictides may be as high as 70 K. In Mg$_{1-x}$Al$_x$B$_2$ the eigen BCS-ratio for $\Delta_x$ is larger than that in 1111, whereas the $T_C^{local}$ is closer to $T_C^0$. The eigen BCS-ratio for the small gap tends to the BCS-limit 3.52 in both 1111 and Mg$_{1-x}$Al$_x$B$_2$ (see Table 1). The gaps ratio $\Delta_L/\Delta_S \approx 3.7$ for iron oxypnictides corresponds to the scaling between both gaps and critical temperature within the range $T_C = 22–50$ K [10,43]. By contrast, in Mg$_{1-x}$Al$_x$B$_2$ the $\pi$-gap does not change with temperature till $T_C \approx 15$ K [17,49,50] (which roughly corresponds to the eigen $T_C^0$ for $\pi$-bands [17,49], thus leading to $\Delta\pi/\Delta\sigma$ increasing.

The dependence of the relative intraband coupling constant (for the small gap) $\lambda_{22}/\lambda_{11}$ on critical temperature for 1111, Mg$_{1-x}$Al$_x$B$_2$, and LiFeAs is shown.
Fig. 4 Experimental temperature dependences for the $\sigma$-gap (solid triangles) and for the $\pi$-gap (open triangles) for $\text{Mg}_2\text{Fe}_{1-x}\text{Al}_xB_2$ with $T_C^{\text{cool}} \approx 21.5$ K. Solid lines show theoretical fitting curves corresponding to two-gap model by Moskalenko and Suhl, dash-dot line show single-gap BCS-like curve. Red dashed lines correspond to eigen BCS-like dependence estimated by us for $\Delta_\pi(T)$ and $\Delta_\sigma(T)$ in a hypothetical case of zero interband coupling. The normalized dependence $\Delta_\pi(T) \times \Delta_\sigma(0)/\Delta_\sigma(0)$ is presented by crossed triangles for comparison. The $\Delta_{L,S}(T)$ dependences were taken from [20].

in Fig. 5. All the data follow the single dependence: $\lambda_{22}$ monotonically grows relatively to $\lambda_{11}$ with $T_C$ decreasing. Such behaviour also agrees with that predicted by the RBCS model. At the same time, the experimental points on the effective interband coupling constants, $\sqrt{\lambda_{L,S}/\lambda_{LL}}$ (open symbols in Fig. 5) obviously form two groups: $\sqrt{\lambda_{L,S}/\lambda_{LL}} = 0.08-0.18$ for Fe-1111 compounds, and 0.03-0.07 for $\text{Mg}_2\text{Fe}_{1-x}\text{Al}_xB_2$. Again, the smallness of the latter constant confirms a weaker interband coupling for $\text{Mg}_2\text{Fe}_{1-x}\text{Al}_xB_2$ in comparison with that for 1111.

In conclusion, we directly measured temperature dependences of the large and the small gap for oxypnictide superconductors GdO$_x$FeAs, Sm$_{1-x}$Th$_x$Fe$_2$As, and LaO$_{1-x}$F$_x$FeAs, for $\text{Mg}_2\text{Fe}_{1-x}\text{Al}_xB_2$, and LiFeAs. The $\Delta_{L,S}$ are well-fitted with a two-band Moskalenko and Suhl system of gap equations within the RBCS model. We estimated relative values of electron-boson coupling constants, and the eigen BCS-ratios for both bands. Our data prove a strong intraband and a weak interband coupling in the studied two-gap superconductors.

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Table 1 Parameters of superconducting state estimated from the $\Delta_{L,S}(T)$ fitting by Moskalenko and Suhl equations. *For LiFeAs, the effective large gap is taken [31].

|                  | GdO$_{0.88}$FeAs | Sm$_{1-x}$Fe$_x$OFeAs | LaO$_{1-x}$Fe$_x$FeAs | (111) | M$_{81-x}$Al$_x$B$_2$ | LiFeAs$^*$ |
|------------------|------------------|------------------------|------------------------|-------|----------------------|-----------|
| $T_C$, K         | 50               | 49                     | 49.5                   | 42    | 26.5                 | 22        |
| $\Delta_L$, meV  | 11.3             | 12                     | 11.8                   | 9     | 6.4                  | 5.4       |
| $\Delta_S$, meV  | 3                | 3                      | 3                      | 2.5   | 2                    | 1.4       |
| $\Delta_L/\Delta_S$ | 3.8             | 3.9                    | 3.6                    | 3.2   | 3.9                  | 3.7       |
| $\Delta_L/k_BT_C$ | 4.3             | 4.8                    | 4.1                    | 4.3   | 4.6                  | 4.4       |
| $\Delta_S/k_BT_S$ | 3.53            | 3.8                    | 3.53                   | 3.53  | 3.53                 | 3.7       |
| $T_C^{local}/T_C$ | 0.83            | 0.81                   | 0.75                   | 0.85  | 0.71                 | 0.81      |
| $T_C^{mod}/T_C$  | 0.9                 | 0.81                   | 0.75                   | 0.85  | 0.83                 | 0.83      |

* For LiFeAs, the effective large gap is taken [31].
