A polarimetric study of asteroids in comet-like orbits

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ABSTRACT

Context. Asteroids in comet-like orbits (ACOs) consist of asteroids and dormant comets. Due to their similar appearance, it is challenging to distinguish dormant comets from ACOs via general telescopic observations. Surveys for discriminating dormant comets from the ACO population have been conducted via spectroscopy or optical and mid-infrared photometry. However, they have not been conducted through polarimetry.

Aims. We conducted the first polarimetric research of ACOs.

Methods. We conducted a linear polarimetric pilot survey for three ACOs: (944) Hidalgo, (3552) Don Quixote, and (331471) 1984 QY1.

Results. We found that Don Quixote and Hidalgo have polarimetric properties similar to comet nuclei and D-type asteroids (optical analogs of comet nuclei). However, 1984 QY1 exhibited a polarimetric property consistent with S-type asteroids. We conducted a backward orbital integration to determine the origin of 1984 QY1, and found that this object was transported from the main belt into the current comet-like orbit via the 3:1 mean motion resonance with Jupiter.

Conclusions. We conclude that the origins of ACOs can be more reliably identified by adding polarimetric data to the color and spectral information. This study would be valuable for investigating how the ice-bearing small bodies distribute in the inner Solar System.

Key words. Polarization - Techniques: polarimetric - Minor planets, asteroids: individual: (944) Hidalgo, (3552) Don Quixote, (331471) 1984 QY1

1. Introduction

A classification between comets and asteroids (the notation is given in Appendix A) is important for investigating the compositional distribution in the present Solar System. In a conventional view, asteroids are distributed in the inner Solar System (i.e., mostly located in the main-belt region with low eccentricities), while comets originate from the outer Solar System (the Kuiper Belt or the Oort Cloud) with high eccentricities.

Because of their different origins, asteroids and comets have been conventionally distinguished by several properties. In terms of appearance, comets show tails and comae by ejecting gas and dust as they approach the Sun. Asteroids generally do not show cometary activity (except active asteroids, Jewitt 2012), so they have a point-source appearance. In terms of the orbital properties, the Tisserand parameter (an approximation derived from the Jacobi integral of the circular restricted three-body problem) with respect to Jupiter ($T_J$) has been employed to discriminate between comets and asteroids. In general, asteroids are dynamically disconnected from Jupiter, while comets are coupled or intersect with the orbit of Jupiter, providing $T_J > 3$ for asteroids and $T_J < 3$ for comets (Kresak 1982; Levison & Duncan 1997). In terms of the optical properties, reflectance spectra and geometric albedos ($p_v$) are used for classification (Licandro et al. 2008, 2011; Kim et al. 2014; DeMeo & Binzel 2008). Typically, comet nuclei have red spectra with low $p_v$ ($p_v = 0.02–0.06$)
Campins & Fernández 2002; Lamy et al. 2004), and asteroids have a wide range of reflectance spectra and geometric albedos ($p_V = 0.02–0.60$, Usui et al. 2011). However, it turns out that this conventional classification could not work for some objects, such as asteroids in comet-like orbits (i.e., asteroids having apparent $T_0 < 3$, hereafter ACOs).

Although dormant comets in the ACO population have been investigated via several methods, such as optical multiband photometry, spectroscopy, and infrared photometry (Fernández et al. 2001, 2005; Kim et al. 2014), few have been studied through polarimetry. Polarimetric observations can provide the polarization degree–phase angle $P_\theta(\alpha)$ profile of targets, where $\alpha$ is the Sun–target–observer angle. In general, the $P_\theta(\alpha)$ profiles of small bodies in the Solar System show negative $P_\theta$ (i.e., light polarized in a parallel direction to the scattering plane) at $\alpha \lesssim \alpha_0 $ and positive $P_\theta$ (i.e., the perpendicularly polarized direction with respect to the scattering plane) at $\alpha \gtrsim \alpha_0 $ (Cellino et al. 2016). Here, $\alpha_0$ is the inversion angle where $P_\theta(\alpha_0) = 0$, and which generally appears at $\alpha \sim 20^\circ$. Then, $P_\theta$ pseudolinearly increases around $\alpha_0$ with a slope of $h$ and shows the maximum polarization degree ($P_{\max}$) at $\sigma_{\max} \sim 100^\circ$. Consequently, the $P_\theta(\alpha)$ profiles are characterized by several key parameters (e.g., the slope $h$, $\alpha_0$, $P_{\max}$). The surface properties (such as albedo and grain size) were conjectured with these parameters. (Geake & Dollfus 1986; Dollfus et al. 1989; Shkuratov & Opanasenko 1992; Lupishko 2018).

In this paper we conducted a polarimetric pilot survey of three ACOs, (944) Hidalgo, (3552) Don Quixote, and (331471) 1984 QY1 (hereafter Hidalgo, Don Quixote, and QY1), to test the potential of polarimetry for ACO research. We chose Don Quixote and QY1 not only because they were bright in 2016–2019, but also because they have a high probability of being Jupiter-family comets (> 96 %, Bottke et al. 2002). Hidalgo is a dormant comet candidate because of its orbital and spectral properties (Hartmann et al. 1987; Tholen 1984). More detailed information on the targets is summarized in Table 1. We describe the observations and data reduction processes in Sect. 2 and observational results in Sect. 3. We discuss the results based on our polarimetry and the dynamical properties and the surface prospects of the polarimetric study for ACOs in Sect. 4.

2. Observations and data analysis

The journal of the observations is given in Table 2. We conducted polarimetry with the 1.6-m Pirka Telescope at the Hokkaido University Observatory (142:5 E, 44:4 N at 151 m above sea level, observatory code number Q33) in Japan from UT 2016 May 25 to 2019 July 22. During this period there were three ACOs (Don Quixote, Hidalgo, and QY1) that were bright enough to be measured by the instrument ($V$-band magnitudes $\lesssim 17$ mag) with sufficiently small errors ($\lesssim 1\%$) at moderately large $\alpha \sim 30^\circ$. Among them, we had an opportunity to observe QY1 at a very large $\alpha$ ($\alpha \approx 100^\circ$). We utilized the visible multispectral imager (MSI) attached to the Cassegrain focus of the 1.6-m Pirka telescope, covering a field of view of $3\times3$ with a pixel resolution of $0^\prime/39$ (Watanabe et al. 2012). We obtained the polarimetric data with $V$-band and $R_C$-band filters. The polarimetric module is optional for MSI, which consists of a rotatable half-wave plate and a Wollaston prism (a polarizing beam splitter), which has the advantage of reducing the influence of time-dependent atmospheric extinction. A polarization mask divides the field of view into two areas of the sky of $3\times3$ $^\prime/07$, and each area produces a data set having ordinary and extraordinary images simultaneously without mixing ordinary and extraordinary signals (Fig. 1). We adjusted an exposure time of 60–180 sec, considering the signal-to-noise ratio at each half-wave plate angle (changed in the sequence of $\theta = 0^\circ$, $45^\circ$, $22.5^\circ$, and $67.5^\circ$).

We analyzed the data in the same manner as in Ishiguro et al. (2017) and other papers using Pirka/MSI (Kuroda et al. 2015, 2021). The raw data were bias-subtracted and flat-fielded using the MSI data reduction package. Cosmic rays were subtracted using the L.A. Cosmic tool (van Dokkum 2001). After preprocessing, we performed aperture photometry to extract the source fluxes from the ordinary and extraordinary parts of objects on the images using the photometry package in the Image Reduction and Analysis Facility (IRAF) and astropy (Astropy Collaboration et al. 2013, 2018) of the Python package. The typical aperture size was $2^\prime$/73–$5^\prime$/85. Additionally, by visual inspection, we excluded the images with background objects within an aperture radius from the center of our targets.

We obtained the linear polarization degree ($P$) and the position angle ($\theta_p$) with the equations

$$P = \sqrt{\left(\frac{Q}{I}\right)^2 + \left(\frac{U}{I}\right)^2}$$ \hspace{1cm} (1)

and

$$\theta_p = \frac{1}{2} \tan^{-1} \left( \frac{U}{Q} \right),$$ \hspace{1cm} (2)

where $I$, $Q$, and $U$ are the Stokes parameters derived from the extracted fluxes (Tinbergen 1996), and $\theta_p$ denotes the polarization position angle with respect to the celestial north. Before deriving $P$ and $\theta_p$ in the above equations, we corrected the polarization efficiency, instrumental polarization, and position angle offset at the given wavelengths (Ishiguro et al. 2017). After the calibration, we calculated the weighted mean of $q$ and $u$ on each date and derived the polarimetric result. To consider the influence of...
random noise in $P$, we applied the following equation (Wardle & Kronberg 1974):

$$P' = \sqrt{P^2 - \sigma_p^2}.$$  \hspace{1cm}  (3)

When $P$ is nearly equal to zero, $\sigma_p^2$ inevitably becomes larger than $P^2$, which makes the value in the root negative. In this case, we regard it as $P = 0$.

Finally, we converted a polarization degree with respect to the scattering plane (the plane constituted by the target, the Sun, and the Earth) with the equations

$$P_t = P' \cos (2\theta_t)$$ \hspace{1cm} (4)

and

$$\theta_t = \theta_P - (\phi \pm 90^\circ),$$ \hspace{1cm} (5)

where $\phi$ is the position angle referring to the scattering plane on the sky and $\theta_t$ is the angle between the measured direction of the strongest electric vector and the normal to the Sun–target–observer plane, following the convention of asteroids and comet polarimetry (e.g., Lupishko 2014). The ± sign in parentheses is chosen to satisfy $0^\circ \leq (\phi \pm 90^\circ) \leq 180^\circ$ (Chernova et al. 1993).

All the preprocessed polarimetric data used are available via CDS\(^1\).

### 3. Results

Table 3 summarizes the weighted mean values of the nightly linear polarimetric result and Fig. 2 shows the polarization phase curve. In the following subsections we describe our findings.

#### 3.1. Characterization of polarization phase curves

To capture the outlines of polarization phase curves, we fit the data using the empirical Lumme–Muinonen function (Lumme & Muinonen 1993; Penttilä et al. 2005). It is given as

$$P_t(\alpha) = h \left( \frac{\sin (\alpha)}{\sin (\alpha_0)} \right)^{c_1} \left( \frac{\cos (\frac{\alpha}{2})}{\cos (\frac{\alpha_0}{2})} \right)^{c_2} \sin (\alpha - \alpha_0),$$ \hspace{1cm} (6)

where $\alpha_0$, $h$, $c_1$, and $c_2$ are free parameters for fitting polarization phase curves. We modify the original Lumme–Muinonen function so that $h$ corresponds to the polarimetric slope at $\alpha = \alpha_0$. We fit the observation data with Eq. (6), employing the Markov chain Monte Carlo (MCMC) method in emcee (Foreman-Mackey et al. 2013, version 3.0.2). We set boundary conditions of $0 < h < 1$, $0 < c_1, c_2 < 10$, and $10^2 < \alpha_0 < 10^4$. The uncertainties of best-fit parameters are derived based on the 16th, 50th, and 84th percentiles of the samples in the marginalized distributions. The script to fit the polarization phase curve is

### Table 1. Orbits and spectral types of our targets

| Target Name | $a$ (au) | $e$ | $i$ (deg) | $T$ (yr) | Spectral type | References |
|-------------|---------|-----|-----------|----|-------------|------------|
| QY1         | 2.35    | 0.89| 14.3      | 2.68| Unidentified (S or Q)\(\text{r}\) | \ldots |
| Don Quixote | 4.26    | 0.71| 31.1      | 2.31| D           | 1, 2       |
| Hidalgo     | 5.73    | 0.66| 42.5      | 2.07| D           | 2          |

**Notes.** (\(\text{r}\)) Semimajor axis, (\(\text{e}\)) Eccentricity, (\(\text{i}\)) Inclination, (\(\text{T}\)) Tisserand parameter with respect to Jupiter, (\(\text{S}\)) See Sect. 4.3. We obtained these elements ($a$, $e$, and $i$) from the web-based JPL Small-Body Database Browser (https://ssd.jpl.nasa.gov/sbdb.cgi).

### Table 2. Observation circumstance

| Target Name | Date     | UT      | Filter | Exptime\(\text{sec}\) | $N$ (sec) | $r$ (au) | $\Delta$ (au) | $\alpha$ (deg) | $\phi$ (deg) |
|-------------|----------|---------|--------|------------------------|-----------|---------|-------------|-------------|-------------|
| QY1         | 2016-May-25 | 12:09–17:20 | $R_C$ | 120–180 | 28 | 0.87 | 0.30 | 111.7 | 42.2 |
|             | 2016-May-27 | 13:22–14:40 | $V$   | 120     | 0.90 | 0.28 | 104.8 | 60.6 |
|             | 2016-May-27 | 12:53–14:19 | $R_C$ | 120     | 0.90 | 0.28 | 104.8 | 60.5 |
|             | 2016-May-28 | 12:55–15:42 | $V$   | 120     | 0.92 | 0.28 | 101.0 | 74.0 |
|             | 2016-May-28 | 13:35–16:26 | $R_C$ | 120     | 0.92 | 0.28 | 101.0 | 74.5 |
|             | 2016-May-29 | 12:58–16:29 | $V$   | 120     | 0.94 | 0.28 | 97.1  | 89.1 |
|             | 2016-May-29 | 12:50–16:16 | $R_C$ | 120     | 0.94 | 0.28 | 97.1  | 89.3 |
|             | 2016-Jun-21 | 12:54–14:38 | $V$   | 60      | 60.3 | 0.52 | 43.4  | 131.3 |
|             | 2016-Jun-21 | 11:25–17:24 | $R_C$ | 60–120  | 56  | 1.33 | 0.52 | 43.4  | 131.3 |
|             | 2016-Jun-24 | 11:20–14:56 | $R_C$ | 60–120  | 32  | 1.38 | 0.58 | 41.2  | 128.8 |
| Don Quixote | 2018-Jul-24 | 17:18–18:09 | $R_C$ | 120–180 | 20 | 1.58 | 1.46 | 38.7  | 254.0 |
|             | 2018-Aug-28 | 15:57–16:16 | $R_C$ | 60      | 20.86 | 1.86 | 140  | 32.5  | 248.4 |
|             | 2018-Sep-14 | 14:53–18:18 | $R_C$ | 60      | 1.89 | 1.40 | 31.5  | 246.5 |
|             | 2018-Sep-02 | 15:57–17:41 | $I_C$ | 120     | 3.69 | 1.90 | 140  | 31.2  | 246.0 |
| Hidalgo     | 2018-Sep-01 | 17:13–17:59 | $R_C$ | 60      | 32   | 2.02 | 1.90 | 29.6  | 266.5 |
|             | 2019-Apr-19 | 13:15–13:59 | $R_C$ | 120     | 3.52 | 4.49 | 22.9 | 119.0 |
|             | 2019-May-30 | 12:13–13:05 | $R_C$ | 120     | 2.82 | 2.92 | 20.3 | 105.4 |
|             | 2019-Jul-22 | 2011:18–11:43 | $R_C$ | 120     | 10.93 | 3.79 | 13.1 | 93.9 |

**Notes.** (\(\text{e}\)) Exposure time for each image in sec, (\(\text{N}\)) Number of exposures used to obtain polarimetric parameters, (\(\text{M}\)) Median geocentric distance in au, (\(\text{C}\)) Median solar phase angle in deg. (\(\text{S}\)) Position angle of the scattering plane in deg. The web-based JPL Horizon system (http://ssd.jpl.nasa.gov/?horizons) was used to obtain these quantities.
Table 3. Polarimetric results

| Target Name | Date       | UT       | Filter | α (deg) | \( P^a \) (%) | \( \sigma p^a \) (%) | \( \theta_p \) (deg) | \( \sigma \theta_p \) (deg) | \( P_\tau^e \) (%) | \( \theta_\tau^e \) (deg) |
|-------------|------------|----------|--------|---------|-------------|----------------|----------------|----------------|----------------|----------------|
| QY1         | 2016-May-25 | 12:09-17:20 | \( R_C \) | 111.7   | 8.48        | 1.08          | -50.95         | 3.64           | 8.45           | -2.63         |
|             | 2016-May-27 | 13:22-14:40 | V      | 104.8   | 8.00        | 0.31          | -31.94         | 1.12           | 7.97           | -2.63         |
|             | 2016-May-27 | 12:53-14:19 | \( R_C \) | 104.8   | 7.97        | 0.21          | -32.76         | 0.75           | 7.92           | -3.33         |
|             | 2016-May-28 | 12:55-15:42 | V      | 101.0   | 8.56        | 0.33          | -19.56         | 1.09           | 8.56           | -4.14         |
|             | 2016-May-28 | 13:35-16:26 | \( R_C \) | 101.0   | 8.48        | 0.27          | -17.20         | 0.90           | 8.46           | -1.88         |
|             | 2016-May-29 | 12:58-16:29 | V      | 97.1    | 7.72        | 0.24          | -4.74          | 0.90           | 7.65           | -3.85         |
|             | 2016-May-29 | 12:50-16:16 | \( R_C \) | 97.1    | 7.64        | 0.27          | -2.19          | 0.99           | 7.63           | -1.56         |
|             | 2016-Jun-21 | 12:54-14:38 | V      | 43.4    | 2.88        | 0.35          | 42.45          | 3.48           | 2.88           | 1.14          |
|             | 2016-Jun-21 | 11:25-17:24 | \( R_C \) | 43.3    | 2.75        | 0.38          | 38.06          | 3.98           | 2.73           | -3.25         |
|             | 2016-Jun-24 | 11:20-14:56 | \( R_C \) | 41.2    | 2.32        | 0.55          | 32.27          | 6.81           | 2.26           | -6.56         |
| Don Quixote | 2018-Jul-24 | 17:18-18:09 | \( R_C \) | 38.7    | 7.64        | 0.37          | -21.48         | 1.39           | 7.50           | -5.50         |
|             | 2018-Aug-28 | 15:57-16:16 | \( R_C \) | 32.5    | 4.65        | 0.71          | -30.40         | 4.39           | 4.43           | -8.80         |
|             | 2018-Sep-01 | 14:53-18:18 | \( R_C \) | 31.5    | 3.72        | 0.44          | -23.74         | 3.41           | 3.72           | -0.25         |
|             | 2018-Sep-02 | 15:57-17:41 | \( I_C \) | 31.2    | 4.16        | 0.63          | -20.19         | 4.32           | 4.12           | 3.85         |
| Hidalgo     | 2018-Sep-01 | 17:13-17:59 | \( R_C \) | 29.6    | 3.47        | 0.12          | -5.52          | 0.97           | 3.46           | -1.99         |
|             | 2019-Apr-19 | 13:15-13:59 | \( R_C \) | 22.9    | 1.16        | 0.14          | 23.45          | 3.49           | 1.14           | -5.51         |
|             | 2019-May-30 | 12:13-13:05 | \( R_C \) | 20.3    | 0           | 0.31          | -11.80         | 49.49          | 0              | -27.22         |
|             | 2019-Jul-22 | 11:18-11:43 | \( R_C \) | 13.1    | 0.91        | 0.51          | -86.37         | 16.03          | -0.91          | 89.75         |

Notes. (a) Nightly averaged linear polarization degree in percent, (b) Error of \( P \) in percent, (c) Position angle of the strongest electric vector in deg, (d) Error of \( \theta_p \) in deg, (e) Polarization degree referring to the scattering plane in percent (see Eq. (3)), (f) Position angle referring to the scattering plane in deg (see Eq. (4)).

![Fig. 2. Phase angle dependence of nightly averaged \( P_\tau \) for three ACOs: (a) Hidalgo, (b) Don Quixote, and (c) QY1. Polarization phase curves using the median of the Monte Carlo samples are shown as the red solid line for \( R_C \) band and the green dashed line for \( V \) band by using Eq. (6). For Hidalgo we plot the \( V \)-band data (open circle) from Fornasier et al. (2006).](https://github.com/Geemjy/Geem_2021_AA)

Available via the GitHub \(^2\) The best-fit parameters with ±1σ uncertainties are summarized in Table 4. With the parameters we show the fitted profiles in Fig. 2. In the figure the polarization phase curves of Don Quixote and Hidalgo are similar to each other, but are different from QY1 in that they have polarimetric slopes steeper than QY1 (i.e., larger \( h \) values). The inversion angle of Hidalgo is determined well to \( \alpha_0 = 18^\circ 87^\circ 62^\circ \). On the contrary, the inversion angles of Don Quixote and QY1 we less precise due to the lack of data in the negative branch, preventing accurate determination (see Table 5), and yet the fitting process would work well because these \( \alpha_0 \) values are typical of general asteroids (i.e., \( \sim 20^\circ \)).

Figure 3 compares the polarization phase curves of three ACOs with a comet nucleus and other types of asteroids. We utilize the \( P_\tau \) data of a bare comet nucleus (209P/LINEAR, Kuroda et al. 2015) and C-, D-, B-, and S-type asteroids (Gil-Hutton et al. 2014, 2017; Ishiguro et al. 2017; Ito et al. 2018; Kuroda et al. 2021; Lupishko 2014; Shimakawa et al. 2018).

In Fig. 3, the distribution of different objects depends mostly on their albedos. Lower albedo objects are distributed on the upper side, while higher albedo objects are distributed on the lower side. We draw the borderline corresponding to \( p_V = 0.1 \) (dash-dotted line) in Fig. 3. The borderline is the straight line whose slope is obtained by putting \( p_V = 0.1 \) in Eq. 7 and starts from \( \alpha = 20^\circ \) (i.e., typical \( \alpha_0 \) of asteroids, Belskaya et al. 2017). It becomes clear that objects with \( p_V < 0.1 \) are located above the borderline. The \( P_\tau \) of Don Quixote, Hidalgo, and the comet nucleus are located on the upper side, indicating that they have consistent albedo values (\( p_V < 0.1 \)). On the other hand, the polarimetric profile of QY1 is similar to that of S-type asteroids as it is below the line for \( p_V = 0.1 \).

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2 https://github.com/Geemjy/Geem_2021_AA
Table 4. Fitting result of polarization phase curves

| Target Name | Filter | $h$ (deg) | $\alpha_0$ (deg) | $c_1$ | $c_2$ | $\alpha_{\text{max}}$ (deg) | $P_{\text{max}}$ (%) |
|-------------|--------|-----------|------------------|------|------|--------------------------|------------------|
| Hidalgo     | $R_C$  | $0.253\pm0.056$ | $18.87\pm0.84$  | $0.893\pm0.418$ | $5.429\pm3.174$ | $\ldots$ | $\ldots$ |
| Don Quixote | $R_C$  | $0.353\pm0.225$ | $22.79\pm3.70$  | $1.017\pm0.871$ | $5.394\pm3.153$ | $\ldots$ | $\ldots$ |
| QY1         | $V$    | $0.129\pm0.042$ | $24.05\pm4.80$  | $0.323\pm0.202$ | $0.377\pm0.258$ | $98.83\pm5.91$ | $8.08\pm3.19$ |
| QY1         | $R_C$  | $0.127\pm0.052$ | $24.87\pm4.68$  | $0.341\pm0.248$ | $0.347\pm0.240$ | $99.79\pm5.26$ | $8.14\pm3.55$ |

Fig. 3. Comparison of $P_{\nu}(\alpha)$ profiles of QY1, Don Quixote, and Hidalgo with asteroids and a bare comet nucleus, 209P/LINEAR, (Kuroda et al. 2015). Each letter (C, B, and S) indicates the taxonomic types. The $P_{\nu}$ value of Hidalgo in Fornasier et al. (2006) is plotted as the triangle marker. We plot the diagnostic line (dash-dotted line) corresponding to $p_{\nu} = 0.1$. Objects with $p_{\nu} \leq 0.1$ are be located on the upper side of the line and vice versa.

Table 5. Results of $\alpha_{\text{ic}}$, $h$, and $p_{\nu}$

| Target Name | $\alpha_{\text{ic}}$ (deg) | $h$ (%/deg) | $p_{\nu}$ | References |
|-------------|-----------------|------------|----------|------------|
| Hidalgo     | $18.87^{+0.62}_{-0.84}$ | $0.253^{+0.042}_{-0.056}$ | $0.050^{+0.017}_{-0.009}$ | $\ldots$ |
| Don Quixote | $22.79^{+0.51}_{-0.70}$ | $0.353^{+0.023}_{-0.198}$ | $0.035^{+0.049}_{-0.014}$ | $\ldots$ |
| QY1         | $24.87^{+0.03}_{-4.68}$ | $0.129^{+0.042}_{-0.099}$ | $0.153^{+0.107}_{-0.022}$ | $\ldots$ |
| S-type asteroids | $20.7^{+0.2}_{-0.2}$ | $0.110^{+0.005}_{-0.005}$ | $0.21^{+0.08}_{-0.08}$ | 1, 2 |
| D-type asteroids | $18.2^{+0.3}_{-0.3}$ | $0.341^{+0.109}_{-0.097}$ | $0.09^{+0.05}_{-0.05}$ | 1, 2 |
| C-type asteroids | $19.4^{+0.1}_{-0.1}$ | $0.387^{+0.037}_{-0.037}$ | $0.07^{+0.04}_{-0.04}$ | 1, 2 |
| Comet nuclei | $\ldots$ | $0.02^{+0.06}_{-0.06}$ | $3$ | |

Notes.

$^{(a)}$ Derived by the observation in $R_C$ band. $^{(b)}$ These $p_{\nu}$ values were derived from $h$ and color. $^{(c)}$ Derived by the observation in $V$ band.

References. (1) Belskaya et al. (2017); (2) Usui et al. (2013); (3) Lamy et al. (2008).
3.2. Derivation of geometric albedo

Since the polarimetric slopes depend on their albedo, as seen in Sect. 3.1, we derive the geometric albedos (\(p_V\)) of ACOs from their slope \(h\). It is well known that the slope \(h\) has a good correlation with \(p_V\). This was first noted by Widorn (1967) and Kenknight et al. (1967). The correlation is expressed with the empirical equation

\[
\log_{10}(p_V) = C_1 \log_{10}(h) + C_2 \tag{7}
\]

where \(C_1\) and \(C_2\) are constants. They have been determined by several research groups (Masiero et al. 2012; Cellino et al. 2015; Lupishko 2018). Here we use \(C_1 = -1.016 \pm 0.010\) and \(C_2 = -1.719 \pm 0.012\) from Lupishko (2018), which uses the most comprehensive data sets obtained by infrared space telescopes and occultations. In addition, although \(C_1\) and \(C_2\) are obtained in \(V\) band, we practically assume that the slope \(h\) is dominantly controlled by the geometric albedo regardless of wavelength (Umemoto 1905) to apply \(C_1\) and \(C_2\) to our data in \(R_C\) band. Substituting the slope \(h\) values in Eq. (7), we computed the geometric albedo values; and the results are summarized in Table 5. The uncertainty of the albedo is calculated based on the uncertainties of \(h\), \(C_1\), and \(C_2\) in Eq. (7). For comparison, we provide the average values or typical range of asteroids and comet nuclei in Table 5.

In the case of Don Quixote and Hidalgo, only geometric albedos in the \(R_C\) band (\(p_{R_C}\)) are derived from our polarimetry. The results are \(p_{R_C} = 0.855_{-0.021}^{+0.072}\) for Don Quixote and \(p_{R_C} = 0.078_{-0.002}^{+0.002}\) for Hidalgo. Since the geometric albedo is defined in the \(V\) band, we should convert them (i.e., \(p_{R_C}\)) to \(V\)-band albedos (i.e., \(p_V\)) using their color indices (\(V - R\)). The applied \(V - R\) values are summarized in Appendix C. The corresponding \(p_V\) values are summarized in Table 5. These \(p_V\) values of Don Quixote and Hidalgo are in the range of the typical \(p_V\) of comet nuclei and C- and D-type asteroids (Lamy et al. 2008; Usui et al. 2013). In contrast, \(p_V\) of QY1 is in the range of typical \(p_V\) of S-type asteroids (Usui et al. 2013). We note that slope \(h\) of Don Quixote and QY1 are derived by extrapolation to the range of \(a < 20'\) where no data is available. Because Eq. (6) used for the fittings is the empirical function (Lunme & Muinonen 1993; Penttilä et al. 2005), polarimetric parameters derived by extrapolation is uncertain. However, we confirm that, while their \(a_0 > 15'\), Don Quixote always shows the slope \(h\) and the albedo (i.e., \(p_V < 0.1\)) compatible with those of D-type asteroids (the optical analog of comet nuclei), whereas QY1 indicates these values are comparable with those of S-type asteroids.

3.3. Slope \(h\) and the color Index \(V - R\)

Although the polarimetric slope \(h\) is a useful proxy of albedo, it is insufficient to distinguish possible dormant comets from C-complex asteroids (C-, F-, and B-types) because comet nuclei (including D-type) and C-complex asteroids have similar albedo values. Therefore, we utilize the color index \(V - R\) together with the slope \(h\). We compare the slopes \(h\) and \(V - R\) of ACOs with those of other asteroids and comet nuclei (Fig. 4). We convert the slope \(h\) of Don Quixote and Hidalgo in the \(R_C\) band to the \(V\) band using their \(V - R\) color indices (Appendix C). In Fig. 4, objects are divided into three major groups: S-type asteroids; C-, F-, and B-type asteroids; and comet nuclei. Because comet nuclei have optical properties (colors and albedos) similar to D-type asteroids, they overlap with each other. Don Quixote and Hidalgo are clearly distinguished from C-type asteroids and are located in a region similar to comet nuclei and D-type asteroids. Meanwhile, QY1 is compatible with S-type asteroids.

4. Discussion

In this study we attempt to extract dormant comets from the ACO list. We conduct a polarimetric pilot survey for three ACOs to test the potentiality and found that two are likely dormant comets, while another is an S-type asteroid. Here we describe the characteristics of these three ACOs in the following subsections.

4.1. (3552) Don Quixote

Don Quixote should be in the class of comets of outer Solar System origin that contain volatile components such as \(\text{H}_2\text{O}\) and \(\text{CO}_2\) ices. This object was discovered in 1983 as an asteroid despite the comet-like orbit \((T_1 < 3\), Weissman et al. 2002\). It has a very elongated orbit with perihelion and aphelion distances of 1.24 au and 7.28 au, respectively. The diameter and geometric albedo are estimated as \(D = 18.4^{+0.3/-0.4}\) km and \(p_V = 0.03_{-0.01}^{+0.02}\) from thermal infrared data taken with the Spitzer Space Telescope, the NASA Infrared Telescope Facility, and the Wide-field Infrared Survey Explorer (WISE) (Momert et al. 2014). It is classified as a D-type asteroid (Tholen 1984; Bus & Binzel 2002; Rayner et al. 2003). Recent telescopic observations at optical and infrared wavelengths confirm that Don Quixote has exhibited weak comet-like activity at heliocentric distances within 3 au (Momert et al. 2014, 2020; Kokhrirova et al. 2021). The activities were not episodic but recurrent, as observed at different perihelion passages in 2009 and 2017–2018. Moreover, a coma and a tail show the excess signal associated with \(\text{CO}_2\) molecules in the Spitzer Space Telescope observation (Momert et al. 2014). For these reasons, there is no doubt that Don Quixote is a volatile-bearing cometary object of outer Solar System origin.

Our polarimetric observation was conducted starting on July 24, 2018, ten days after the cessation of activity was confirmed by Kokhrirova et al. (2021). We thus measure the polarization degree of the bare nucleus. Without using a space infrared telescope or a large telescope with a mid-infrared instrument, we derive the albedo of \(p_V = 0.035_{-0.014}^{+0.049}\) which is consistent with the result from the Spitzer Space Telescope (Momert et al. 2014). The comet-like optical properties are seen in the polarimetric slope–color plot (Fig. 4). The polarimetry of Don Quixote thus becomes a benchmark for demonstrating the validity of dormant comet extraction using the polarimetric slope–color plot.

4.2. (944) Hidalgo

Since its discovery in 1920 Hidalgo has never exhibited comet-like activity. Nevertheless, it is suspected to be a dormant comet for the reasons described here. This object has a very elongated orbit with perihelion and aphelion distances of 1.95 au and 9.53 au. Thus, this object not only intersects Jupiter’s orbit (the semimajor axis \(a = 5.20\) au), but also reaches Saturn’s orbit (\(a = 9.55\) au) around its aphelion. The diameter and geometric albedo are estimated as \(D = 61.4 \pm 12.7\) km and \(p_V = 0.028 \pm 0.006\) using WISE data and \(D = 52.45 \pm 3.60\) km (Licandro, J. et al. 2016) and \(p_V = 0.042 \pm 0.007\) using AKARI data (Usui et al. 2011). The albedo value we derived via polarimetry is \(p_V = 0.050_{-0.009}^{+0.017}\). These result are in the albedo range of comet nuclei. Additionally, Hidalgo has a spectrum of D-type asteroids (Tholen 1984;
Fig. 4. Polarimetric slope $h$ and $V - R$ plot of Hidalgo, Don Quixote, and QY1 with different types of asteroids and comet nuclei. Each letter (C, B, S, and D) indicates the taxonomic asteroid type. We label (7968) Elst-Pizarro as a B-type asteroid (Licandro et al. 2011). More details and references are given in Sect. 3.3 and Appendix C.

Bus & Binzel 2002; Rayner et al. 2003). All the results support the idea that Hidalgo is a strong candidate for a dormant comet.

As shown in Table 3 and Fig. 2, Hidalgo is observed around $\alpha \sim 20^\circ$, making it possible to derive the polarimetric inversion angle ($\alpha_0$). From the fitting we derive $\alpha_0 = 18.87^{+0.6}_{-0.64}$. The derived $\alpha_0$ of Hidalgo is slightly smaller than for the majority of asteroids, but consistent with the typical $\alpha_0$ value of D-type asteroids (i.e., $\alpha_0 = 18.2 \pm 0.3$, Belskaya et al. 2017), strengthening the result that it is D-type. Meanwhile, there are two reports regarding the $\alpha_0$ of objects showing comet-like activity derived without gas or dust contamination: 2P/Encke, which indicates $\alpha_0 \sim 13^\circ$ in the $R$ band (Boehnhardt et al. 2008), and (7968) Elst-Pizarro, which indicates $\alpha_0 = 17.6 \pm 2^\circ$ in the $R$ band and $\alpha_0 = 17.0 \pm 1^\circ$ in the $V$ band (Bagnulo et al. 2010). These $\alpha_0$ values are smaller than typical asteroids and are nearer to F-type asteroids ($\alpha_0 \sim 15^\circ$, Belskaya et al. 2005; Cellino et al. 2016; Belskaya et al. 2017).

Bagnulo et al. (2010) further note that three F-like asteroids, (4015) Wilson-Harrington (C- or F-type; Tholen 1984), (3200) Phaethon (B- or F-type; Tholen & Barucci 1989; Licandro et al. 2007), and (155140) 2005 UD (B- or F-type; Kinoshita et al. 2007), have evidence of dust emissions, and they point out the association between small $\alpha_0$ asteroids and dust-ejecting objects. Although there are only two report (2P/Encke and (7968) Elst-Pizarro) that indicated the small $\alpha_0$, it is interesting to study the small $\alpha_0$ objects from the viewpoint of dust-ejecting objects. It is also a recent discovery that OSIRIS-REx witnesses dust ejection from (101955) Bennu (Lauretta et al. 2019). From polarimetry it is reported that the asteroid has a small $\alpha_0$ (i.e., $\alpha_0 = 17.88 \pm 0^\circ.40$, Cellino et al. 2018).

In this paper, however, we consider that the application of $\alpha_0$ may not be a decisive factor to distinguish comets (including dust-emitting objects) from asteroids. Because the purpose of this study is to discriminate icy cometary objects of outer Solar System origin from asteroidal objects, we should regard the small $\alpha_0$ objects (7968) Elst-Pizarro (a Themis family member, Hsieh et al. 2004) and (101955) Bennu (an asteroid possibly originating from the Polana-Eulalia family complex, Bottke et al. 2015) as asteroids rather than comets. We note that our designations of comets and asteroids in this paper (Appendix A) do not contradict the idea of Bagnulo et al. (2010). As described in Belskaya et al. (2005), highly reflective particles with a size comparable to the optical wavelength may affect the small $\alpha_0$ for 2P/Encke and (7968) Elst-Pizarro. As the number of $\alpha_0$ measurements for dust-ejecting objects increases in the future, it is expected that there may be a finding regarding the surface state of objects with small $\alpha_0$.

Thus, it is very likely that Hidalgo is a dormant comet, even if it does not have a small $\alpha_0$.

4.3. (331471) 1984 QY1

We conclude that QY1 is most likely an asteroid because of its high albedo ($P_V = 0.153^{+0.107}_{-0.042}$). The $P_{\text{max}}$ value (8.14$^{+3.41}_{-3.55}$ % in the $RC$ band) is significantly lower than that of the 209P/LINEAR nucleus. Recent SMASH II observation data indicate that QY1 is an $S_q$-type or Q-type asteroid when using the Bus-Demo classification tool. The spectrum displays absorptions of approximately 0.9 $\mu$m and 1.9 $\mu$m, typical of these types of asteroids (DeMeo et al. 2009a; Rayner et al. 2003). Thus, these observations (including our polarimetry) indicate that QY1 is an S-complex asteroid.

The polarimetry of QY1 provides a rare opportunity for deriving the surface particle size. Taking advantage of our observa-
It is known that $P_{\text{max}}$ depends on the geometric albedo (Umow 1905) and the particle size (Geake & Dollfus 1986). Shkuratov & Opanasenko (1992) derived a formula to estimate the particle size $d$ (in μm) from $P_{\text{max}}$ and a sort of albedo:

$$d = 0.03 \exp \left(2.9 \log_{10}(100A) + 0.845 \log_{10}(10P_{\text{max}})\right), \quad (8)$$

where $A$ denotes an albedo at $\alpha = 5^\circ$. Applying the intensity ratio $(I(0)/3)/I(5^\circ) = 1.44 \pm 0.04$ for S-type asteroids; Belskaya & Shevchenko (2000), we obtain $A = 0.11 \pm 0.03$ for QY1. Substituting $A$ in Eq. (8), we obtain an estimate of the particle diameter, $d \approx 70$ μm. The size is slightly larger than the S-type asteroid (4179) Toutatis ($\lesssim 50–80$ μm, Ishiguro et al. 1997; Bach et al. 2019), but smaller than the near-Sun Q-type asteroid (1566) Icarus (100–130 μm, Ishiguro et al. 2017). We note that Eq. (8) should be applied to asteroids carefully since a formula is established on the lunar samples. Even so, we use Eq. (8), which is the same method as in previous studies for comparison.

Lastly, we consider the paradoxical problem that the S-type asteroid QY1 has a comet-like orbit. According to a dynamical study of near-Earth objects (Bottke et al. 2002), QY1 has a 96.1% probability of Jupiter-family comets origin, which was one of the highest-potential dormant comet candidates in the list. Since then, its orbital elements have been updated thanks to the accumulation of astrometric observations, yet QY1 has $T_J \approx 2.68$, which is significantly smaller than the criterion of $T_J = 3$. From the revised semimajor axis of $a \approx 2.497$ au we note that QY1 is in a 3:1 mean motion resonance (MMR) with Jupiter (i.e., $a_{1,1} \approx 2.50 \pm 0.03$ au). As pointed out in Kim et al. (2014) and Tancredi (2014), $T_J$ must be treated carefully when considering origins. Main-belt asteroids in resonance should experience increasing orbital eccentricity to be transported into the near-Earth region (e.g., Morbidelli et al. 2002). QY1 has likely been injected into the current comet-like orbit by means of the 3:1 MMR with Jupiter. To confirm this hypothesis, we conduct a backward dynamical simulation of QY1 considering the gravity of eight planets and the Sun (Fig. 5). We employ the Mercury 6 integrator for the simulation (Chambers 1999). We generate 200 clones with the orbital elements of QY1 within the 1σ range at the current epoch, considering their orbit covariances (quoted from the JPL Small-Body Database Browser site$^3$). The applied orbital elements and their uncertainties are summarized in Table 6. We integrate these parameters to 800 years in the past with a time step of 8 days, considering the gravitational forces of the Sun and eight planets but ignoring the Yarkovsky force. As shown in Fig. 5, although the $T_J$ values disperse before $-1500$ years, there is a general trend that $T_J$ values continue decreasing over time ($\Delta T_J \approx -0.1$ for 8000 years). Based on this dynamic integration and our polarimetric results, QY1 would be an object of main-belt origin rather than outer Solar System origin. This result is consistent with the fact that S-complex asteroids are dominant in the 3:1 MMR (45%, Kuroda et al. 2014). For confirmation, we examine the possible source regions using the updated source region probability models (Greenstreet et al. 2012; Granvik et al. 2018) and find that QY1 has a high possibility ($\approx 60\%$) of main-belt origin in 3:1 MMR and a very low probability ($\approx 3\%$) of Jupiter-family comets origin using the updated orbital elements in Table 6.

4.4. Potentiality of polarimetry for ACO research

Finally, we describe the effectiveness of polarimetric observations in ACO research. The discrimination of dormant comets from the ACO population is challenging because both have a point-source appearance. The geometric albedos and reflectance spectra (or color indices) have been considered for discrimination. Comet nuclei have featureless and reddish colors due to irradiated organic materials on their surface (Meech et al. 2004; Licandro et al. 2011), while asteroids have a wide variety of colors (Tholen & Binzel 1989; Binzel et al. 2004). Similarly, comet nuclei have low albedos (typically $P_V = 0.02–0.06$, Campins & Fernández 2002; Lamy et al. 2004), while asteroids have a wide range of albedos ($P_V = 0.02–0.60$, Usui et al. 2011). D-type asteroids have optical properties similar to those of comet nuclei so they are indistinguishable by spectroscopic or photometric observation (DeMeo et al. 2009b; Licandro et al. 2011).

To date, geometric albedos of asteroids are derived mostly by radiometry. In the radiometric method, albedo values are derived from the combination of absolute magnitudes and sizes obtained via a thermal model with observation data. According, albedo values derived by radiometry have inherent uncertainties related to the applied thermal model and optical magnitudes. In addition, the use of mid-infrared observation facilities (e.g., space telescopes, such as AKARI, IRAS, and Spitzer, or ground-based telescopes with a mid-IR camera, such as SUBARU/COMICS) is becoming difficult (as of July 2021). On the other hand, because polarimetric instruments are less expensive than these infrared instruments, they are installed in a relatively large number of small and intermediate-sized telescopes. Using such instruments, albedo estimations, which were conventionally performed in infrared space telescopes or large telescope facilities on the ground, are possible. Since albedos can be obtained directly from polarimetric parameters using the empirical equation, no additional information is required (Widorn 1967; Kenknight et al. 1967; Cellino et al. 2012; Cellino et al. 2015). Additionally, the constant parameters for deriving albedos from polarimetry continue to be updated and are becoming more reliable (Masiro et al. 2012; Cellino et al. 2015; Lupishko 2018). In addition, polarimetry with a polarizing beam splitter is highly feasible even under variable conditions, canceling out variable weather conditions to produce reliable results.

Fig. 5. Time evolution of the Tisserand parameter ($T_J$) with respect to Jupiter of QY1. $T_J$ decreases by 0.1 over ~8000 years, which supports that QY1 would be transported from the main-belt region. Each gray line represents different clones whose current orbital elements follow a Gaussian distribution around the average values within their standard deviations (Table 6). The black line represents the results for a particle with the average orbital elements at Epoch 2459396.5 (2021-07-01.0).

$^3$ https://ssd.jpl.nasa.gov/
Table 6. Orbital elements of QY1 at Epoch 2459396.5 (2021-07-01.0)

| \( a \) (au) | \( e \) | \( i \) (deg) | \( q \) (deg) | \( \theta \) (deg) | \( M \) (deg) |
|------------|--------|-------------|-------------|---------------|----------|
| ±8.660 × 10^{-9} | ±2.001 × 10^{-8} | ±5.270 × 10^{-6} | ±2.192 × 10^{-5} | ±2.240 × 10^{-5} | ±2.865 × 10^{-6} |

Notes. \((a)\) Semimajor axis in au, \((b)\) Eccentricity, \((c)\) Inclination in deg, \((d)\) Mean argument of perihelion in deg, \((e)\) Longitude of the ascending node in deg, \((f)\) Mean anomaly in deg.

We obtained these elements from the web-based JPL Small-Body Database Browser (https://ssd.jpl.nasa.gov/sbdb.cgi).

In the future it is expected that a large number of ACOs will be discovered by large systematic surveys, especially by the Vera C. Rubin Observatory (previously known as the Large Synoptic Survey Telescope, LSST; Vera C. Rubin Observatory LSST Solar System Science Collaboration et al. 2021). Early follow-up polarimetric observations with a small or intermediate-sized telescope with a polarimetric instrument are expected to provide an overview of the dormant comet population lurking in the inner Solar System. Our work will be helpful in that we demonstrated the effectiveness and potentiality of polarimetry by conducting this ACO pilot survey for three objects.

5. Summary

We conducted a polarimetric pilot survey for three ACOs (Don Quixote, Hidalgo, and QY1). These three ACOs have a \( T_J \) value significantly smaller than three, and they were recognized as highly possible dormant comet candidates (Hartmann et al. 1987; Bottke et al. 2002). We obtain the polarization phase curve to conjecture their origins together with color information from previous studies. Our major findings are the following:

1. Don Quixote and Hidalgo show polarimetric and color profiles similar to those of comet nuclei and D-type asteroids. Their albedos derived by our polarimetric data are in the range of comet nuclei.
2. Our result of Don Quixote is consistent with the fact that the object indicated recurrent comet-like activities around its perihelion passages. Hidalgo is also likely a dormant comet.
3. The polarimetric profile of QY1 was unexpected, showing a profile similar to S-type asteroids. We find from the dynamical simulation that QY1 was transported from the main belt via the 3:1 mean motion resonance with Jupiter.
4. QY1 has \( 8.08^{+3.19}_{-1.11} \% \) in the \( V \) band and \( 8.14^{+3.41}_{-3.55} \% \) in the \( R_C \) band. From the \( P_{\text{max}} \) values we obtain an estimate of the particle diameter on the surface of QY1 of \( d \approx 70 \mu m \).

The remaining issue is the polarimetric inversion angle (\( \alpha_0 \)). Hidalgo’s \( \alpha_0 \) is in the range of D-type asteroids and the active asteroid (7968) Elst-Pizarro, but out of 2P/Encke’s range. Further polarimetric observations of comet nuclei and ACOs around the inversion angle are required to determine the inconsistency.

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Appendix A: Usage of the terms comets and asteroids

Here we describe the designations of comets and asteroids adopted throughout this paper.

Comets and asteroids have been distinguished from several viewpoints (such as their appearance, composition, and orbital properties). If a small body of the Solar System indicates activity accompanied by a coma and a tail, it is conventionally regarded as a comet; otherwise, it is regarded as an asteroid. From their composition, asteroids consist mostly of refractory components with a small amount of volatiles (or without volatiles), while comets are rich in volatile components and refractory components.

Comets and asteroids are also distinguished by their orbital properties. Comets are thought to migrate from the outer Solar System (i.e., the Kuiper Belt or the Oort Cloud) via dynamic interactions with Jovian planets, and to exhibit comet-like activities when they receive extra solar radiation that causes ice sublimation to form comae and tails. Such objects from the outer Solar System intersect with Jovian planets and have Tisserand parameter values $T_1 < 3$. On the other hand, asteroids are dynamically disconnected from Jovian planets and have $T_1 > 3$ (Levison & Duncan 1997).

These comet-asteroid discrimination methods do not always work, however. For example, 2P/Encke contains icy volatile components (e.g., H$_2$O and CO$_2$, Reach et al. 2013) showing regular activity, but has the Tisserand parameter $T_1 = 3.03$ (i.e., an asteroidal orbit). It is considered that 2P/Encke has the current asteroidal orbit due to the nongravitational effect (acceleration by sublimation of ice) and the gravitational interaction with planets (Levison et al. 2006). Furthermore, after discovering the so-called main-belt comets (comets in the main asteroidal belt with $T_1 > 3$), the distinction between comets and asteroids became ambiguous (Hsieh & Jewitt 2006). The recent discovery of very red asteroids (similar to Kuiper Belt objects) further complicates the designations (Hasegawa et al. 2021).

We were motivated to study ACOs by pioneering research: Fernández et al. (1997), DeMeo & Binzel (2008), Licandro et al. (2008), and Kim et al. (2014). ACOs are asteroids with comet-like orbits ($T_1 < 3$), and most ACOs are thought to be dormant (or low activity) comets that are at the last stage of the evolution of the bodies from the Kuiper Belt or the Oort Cloud, although there are some asteroids transported to the current orbits via mechanisms such as the Yarkovsky effect (Morbidelli et al. 2002; Kim et al. 2014). Since the purpose of this study is to distinguish comets from ACOs, throughout this paper we refer to objects originating from or in the main belt as asteroids and objects from the Kuiper Belt or the Oort Cloud as comets.

Appendix B: Photometry of QY1

We conducted these observations to detect a signature of comet-like activity. A series of photometric observations were made at three observatories: the Okayama Astrophysical Observatory (OAO), the Ishigakijima Astronomical Observatory (IAO), and the Observatoire de Haute-Provence (OHP). The detailed circumstances of the observations are given in Table B.1.

The OAO is located atop Mt. Chikurinji, Okayama Prefecture, Japan (133°35'36"E, 34°34'33"N, 360 m). We performed observations on three nights on UT May 2–5, 2016, using the Multicolor Imaging Telescopes for Survey and Monstrous Explosions (MITSuME) with three Alta U6 cameras (1024 × 1024 pixels) attached to the 50 cm telescope. The IAO is located on Ishigaki Island, Okinawa Prefecture, Japan (124°08'21"E, 24°22'22"N, 197 m). We observed the target asteroid for seven nights on UT May 26–June 12 2016. We used the 105 cm Murikabushi Cassegrain telescope and MITSuME. The MITSuME at IAO was identical to the system at OAO. The OHP is located in Alpes-de-Haute-Provence, Saint-Michel-l’Observatoire, France (5°42'48"E, 43°55'51"N, 650 m). We made observations on three nights on UT August 1–3 2016. We utilized a 120 cm telescope (focal length of 7.2 m) and an Andor Ikon L. 936 camera (2048 × 2048 pixels). The fields of view and pixel scales of these instruments are $12'3 × 12'3 (0''72 pixel$^{-1}$)$ at IAO, $26'0 × 26'0 (1'53 pixel$^{-1}$)$ at OAO, and $13'1 × 13'1 (0''38 pixel$^{-1}$)$ at OHP.

We made a plot of the light curve applying the rotation periods in Warner & Benisheik (2016), where two rotational periods are suggested: $P_1 = 45.5$ hours and $P_2 = 36.6$ hours (Fig. B.1). $P_1$ is the best candidate of the main period. The uncertainty of the period of 0.5 hours is quoted. From our light curve data, the modulation of $P_1$ is clearly seen, but the modulation of $P_2$ is not, probably because our amount of data may not be sufficient to find it.

The observations at OHP were conducted approximately two months after the observations at OAO and IAO. The accuracy of the rotational period (0.5 hours) is not sufficient to compare the OHP data with the others, so we do not plot the OHP data in Fig. B.1. The magnitudes at OHP, $m_R(70') = 17.20–17.65$ mag, are in the range of the maximum and minimum magnitudes in Fig. B.1, so it is likely that the phase angle correction with $b$ works well for the OHP data. This supports the validity of our estimate for the geometric albedo. The reduced magnitude of QY1 in Fig. B.1 is available at the CDS$^4$.

Appendix C: Derivation of spectral gradients in Fig. 4

In Sect. 3.3 we plotted the polarimetric slope $h$ and the color index $V − R$ for three ACOs, asteroids, and comet nuclei (Fig. 4). We used the $h$ values of asteroids provided in the catalog of the asteroid polarization curves (Gil-Hutton et al. 2017). The applied slope $h$ values from the catalog are determined in the $V$ band. Because of the lack of $h$ data for D-type asteroids, we computed $h$ values from $p_V$ values of 267, 1542, 2246, 2569, 2872, 3248, and 4744 by Eq. (7). The albedos of these D-type asteroids are obtained from Usui et al. (2011), Nugent et al. (2016), and Tedesco et al. (2004). If there is multiple albedo information in these catalogs, the averaged values are calculated and used for the plot. The $V − R$ of asteroids and ACOs are derived using the Small Main-Belt Asteroid Spectroscopic Survey (SMASS) data (Bus & Binzel 2002; Rayner et al. 2003). From SMASS spectra, we calculated the normalized spectral gradient ($S'$) defined as

\[ m_R(70') = m_R - 5 \log_{10} (r_\Delta) + b(\alpha - 70') , \]  

where the phase coefficient of $b = 0.032$ was assumed, which is a predicted value for an object with $p_V = 0.178$ (see the empirical equation on page 99, Belskaya & Shevchenko 2000).

We made a plot of the light curve applying the rotation periods in Warner & Benisheik (2016), where two rotational periods are suggested: $P_1 = 45.5$ hours and $P_2 = 36.6$ hours (Fig. B.1). $P_1$ is the best candidate of the main period. The uncertainty of the period of 0.5 hours is quoted. From our light curve data, the modulation of $P_1$ is clearly seen, but the modulation of $P_2$ is not, probably because our amount of data may not be sufficient to find it.

The observations at OHP were conducted approximately two months after the observations at OAO and IAO. The accuracy of the rotational period (0.5 hours) is not sufficient to compare the OHP data with the others, so we do not plot the OHP data in Fig. B.1. The magnitudes at OHP, $m_R(70') = 17.20–17.65$ mag, are in the range of the maximum and minimum magnitudes in Fig. B.1, so it is likely that the phase angle correction with $b$ works well for the OHP data. This supports the validity of our estimate for the geometric albedo. The reduced magnitude of QY1 in Fig. B.1 is available at the CDS$^4$.
Fig. B.1. Light curves of $R_C$ band (top) and $I_C$ band (bottom) produced assuming a rotational period of $P_1 = 45.5$ hours (left column) and $P_2 = 36.6$ hours (right column) (see Warner & Benishek 2016). The horizontal axes indicate the rotational phase, and the vertical axes indicate the magnitudes viewed from $n_0 = \Delta = 1$ au at $\alpha = 70^\circ$, assuming a phase slope parameter $b = 0.032$ mag/deg.

Table B.1. Observation circumstance of photometric data

| Date       | UT        | Telescope | Filter | Exptime$^a$ (sec) | $N^b$ (au) | $\rho^c$ (au) | $\Delta^d$ (deg) | $\alpha^e$ (deg) |
|------------|-----------|-----------|--------|-------------------|-----------|---------------|------------------|------------------|
| 2016-May-26 | 12:33–13:09 | IAO       | $g', R_C, I_C$ | 30 | 76 | 0.88 | 0.29 | 108.6 |
| 2016-May-27 | 11:15–14:03 | IAO       | $g', R_C, I_C$ | 20 | 476 | 0.90 | 0.28 | 105.0 |
| 2016-Jun-02 | 11:39–17:48 | OAO       | $g', R_C, I_C$ | 120 | 320 | 1.01 | 0.28 | 82.1 |
| 2016-Jun-02 | 13:05–14:17 | IAO       | $g', R_C, I_C$ | 20 | 18 | 1.01 | 0.28 | 82.2 |
| 2016-Jun-03 | 11:14–17:43 | OAO       | $g', R_C, I_C$ | 120 | 350 | 1.03 | 0.29 | 78.5 |
| 2016-Jun-03 | 11:47–17:16 | IAO       | $g', R_C, I_C$ | 20 | 384 | 1.03 | 0.29 | 78.5 |
| 2016-Jun-04 | 13:34–16:58 | IAO       | $g', R_C, I_C$ | 20 | 222 | 1.05 | 0.29 | 75.1 |
| 2016-Jun-05 | 11:47–16:20 | OAO       | $g', R_C, I_C$ | 120 | 164 | 1.07 | 0.30 | 72.0 |
| 2016-Jun-08 | 13:34–15:52 | IAO       | $g', R_C, I_C$ | 20 | 262 | 1.12 | 0.33 | 63.4 |
| 2016-Jun-12 | 13:31–14:55 | IAO       | $g', R_C, I_C$ | 20 | 82 | 1.19 | 0.38 | 54.8 |
| 2016-Aug-01 | 20:50 | OHP       | $R_C$ | 300 | 1 | 1.90 | 1.39 | 31.3 |
| 2016-Aug-02 | 20:23–20:29 | OHP       | $R_C$ | 300 | 2 | 1.91 | 1.41 | 31.2 |
| 2016-Aug-03 | 20:09–20:19 | OHP       | $R_C$ | 300 | 3 | 1.92 | 1.43 | 31.0 |

Notes. The observation circumstance of light curve data taken at Okayama Astrophysical Observatory (OAO) and Ishigakijima Astrophysical Observatory (IAO). We used the web-based JPL Horizon system (http://ssd.jpl.nasa.gov/horizons) to obtain these quantities. $^a$ Exposure time in sec. $^b$ Number of data obtained. $^c$ Median heliocentric distance in au. $^d$ Median geocentric distance in au. $^e$ Median solar phase angle in deg.

\[
S' = \left( \frac{dS}{d\lambda} \right) S, \tag{C.1}
\]

where $S$ is the $\lambda$-dependent reflectance, and $S$ is the average $S$ in the wavelength range of $d\lambda$. Here the $dS/d\lambda$ values were calculated by the linear fitting of SMASS spectra between 5,500 Å and 6,500 Å. The derived $S'$ values were converted to $V - R$ values by using Eq. (2) in Jewitt (2002). We obtained $V - R = 0.49 \pm 0.01$ for Don Quixote and $V - R = 0.48 \pm 0.01$ for Hidalgo.

Because there is no optical spectrum for QY1, we derived it using our photometric data ($g'$-, $R_C$-band). The value of $S'$ of QY1 is derived as

\[
\log_{10}(S') = \frac{m_1 - m_{\text{phot}}}{-2.5} \tag{C.2}
\]
\[ S' = \left( \frac{S_{Rc} - S_{d'}}{A_{Rc} - A_{d'}} \right) \left( \frac{S_{Rc} + S_{d'}}{2} \right), \] (C.3)

where the subscript \( \lambda \) denotes the effective wavelength of filters, and \( m_R \) and \( m_{Rc} \) are the apparent magnitudes of the object and the Sun at wavelength \( \lambda \), respectively. Here, we use \( m_{Rc} = -27.15 \) mag and \( m_{Rc} = -26.34 \) mag (Willmer 2018) and \( A_{Rc} = 6480 \) Å and \( A_R = 4710 \) Å. With these parameters we derived the \( V - R \) of QY1 as \( V - R = 0.46 \pm 0.03 \).

Similarly to the D-type asteroids, the slope \( h \) values of comet nuclei were computed from their albedos. The geometric albedos and \( V - R \) or \( (S') \) of comet nuclei were obtained from various sources (Jewitt 2002; Meech et al. 2004; Abell et al. 2005; Campins et al. 2006; Fernández et al. 2006; Lamy et al. 2008; Tubiana et al. 2008; Li et al. 2013). For \( 2P/\text{Encke} \) and \( (7968) \text{ Elst-Pizarro} \), we referred to the slope \( h \) values in Boehnhardt et al. (2008) and Bagnulo et al. (2010).