Retinal Vascular Fractal Dimension, Childhood IQ, and Cognitive Ability in Old Age: The Lothian Birth Cohort Study 1936

Adele M. Taylor1, Thomas J. MacGillivray2,3,4*, Ross D. Henderson1, Lasma Ilzina1, Baljean Dhillon5, John M. Starr6,7, Ian J. Deary1,6*

1 Department of Psychology, University of Edinburgh, Edinburgh, United Kingdom, 2 Centre for Clinical Brain Sciences, University of Edinburgh, Edinburgh, United Kingdom, 3 Clinical Research Imaging Centre, University of Edinburgh, Edinburgh, United Kingdom, 4 Clinical Research Facility, University of Edinburgh, Edinburgh, United Kingdom, 5 Department of Ophthalmology, Princess Alexandra Eye Pavilion, Edinburgh, United Kingdom, 6 Centre for Cognitive Ageing and Cognitive Epidemiology, University of Edinburgh, Edinburgh, United Kingdom, 7 Alzheimer Scotland Dementia Research Centre, University of Edinburgh, Edinburgh, United Kingdom

* I.Deary@ed.ac.uk (IJD); T.J.MacGillivray@ed.ac.uk (TJM)

Abstract

Purpose
Cerebral microvascular disease is associated with dementia. Differences in the topography of the retinal vascular network may be a marker for cerebrovascular disease. The association between cerebral microvascular state and non-pathological cognitive ageing is less clear, particularly because studies are rarely able to adjust for pre-morbid cognitive ability level. We measured retinal vascular fractal dimension ($D_f$) as a potential marker of cerebral microvascular disease. We examined the extent to which it contributes to differences in non-pathological cognitive ability in old age, after adjusting for childhood mental ability.

Methods
Participants from the Lothian Birth Cohort 1936 Study (LBC1936) had cognitive ability assessments and retinal photographs taken of both eyes aged around 73 years ($n = 648$). IQ scores were available from childhood. Retinal vascular $D_f$ was calculated with monofractal and multifractal analysis, performed on custom-written software. Multiple regression models were applied to determine associations between retinal vascular $D_f$ and general cognitive ability ($g$), processing speed, and memory.

Results
Only three out of 24 comparisons (two eyes × four $D_f$ parameters × three cognitive measures) were found to be significant. This is little more than would be expected by chance. No single association was verified by an equivalent association in the contralateral eye.
Conclusions

The results show little evidence that fractal measures of retinal vascular differences are associated with non-pathological cognitive ageing.

Introduction

Cerebrovascular disease is a major cause of cognitive dysfunction, contributing to cognitive impairment in individuals with and without dementia [1,2]. No single set of cognitive disorders characterise cerebrovascular disease [3], and due to difficulties in viewing the cerebral small vessels in vivo, the true burden of cerebral microvascular disease on cognitive function is still poorly understood [4].

The homology of the retinal and cerebral microvasculatures has led researchers to investigate the potential of the retinal microvasculature as a marker of cerebral microvascular state [5]. The vascular network is designed for optimal hemodynamic and distributive functions [6,7] and variation in retinal vascular parameters, such as vessel calibre and branching geometry, may signify a deviation from this. It follows that these retinal changes are a potential marker of cerebrovascular abnormality and disease.

Retinal imaging allows non-invasive, in vivo assessment of the state of the vasculature [8], and is widely used to study systemic vascular disease [9–11]. Some clinical and population-based studies show that retinal microvascular abnormalities are associated with recognised signs of cerebral microvascular pathology, including cerebral microbleeds [12], white matter lesions [13,14], and brain infarcts [15,16]. Importantly, retinal signs are also related to ability in a range of cognitive domains [17–20], and with increased risk of cognitive impairment [21,22] and dementia [23]. Ding et al [24] provided a systematic review of this area. The most consistent associations have been found in studies investigating advanced retinal and cognitive abnormalities, such as those using qualitative measures of retinal abnormality, specifically severe retinopathy, and in those investigating associations with cognitive dysfunction and dementia rather than differences in ‘normal’ cognitive ability. Associations have been weaker and less consistent for less severe retinal abnormalities, quantitative retinal measures, and for non-impaired cognitive function. Combined with the inconsistency in sensitivity and robustness of cognitive measures used across the studies, as yet, there is little hard evidence that retinal vessel differences are associated with non-impaired cognitive ability in older age.

Recently, researchers have attempted to quantify retinal vascular changes using fractal analysis. This method summarises the global complexity of retinal vascular branching, combining information about vessel widths, vessel tortuosity, and branching geometry and density, to give a single dimensionless quantity: the fractal dimension ($D_f$) [25]. Applied to retinal images, it has potential to be a highly sensitive gauge of microvascular disease. A suboptimal retinal vascular network increases energy costs and reduces efficiency of metabolic transport; microvascular health is maintained by both adequate vessel diameters and optimal branching architecture [26]. Low $D_f$ values, which deviate from the idealised space-filling state of an “optimized” vascular branching network ($D_f = 1.7$) [27–30] have previously been associated with stroke [31], diabetic retinopathy [32], coronary heart disease mortality [26], cognitive dysfunction [22], and dementia [23]. However, it is not known if deviations from optimality are also related to differences in non-pathologic cognitive ageing. Furthermore, most studies have relied on monofractal analysis; a method which has generally achieved limited success [33]. Greater success has been reported by studies using multifractal techniques which
characterise the retinal vasculature with a hierarchy of exponents rather than a single fractal dimension [34].

An important methodological point is that few studies to date have made adjustments for differences in prior cognitive ability when investigating the association between retinal vascular parameters and cognitive ability later in life. This is important because childhood cognitive ability accounts for a large proportion of variance in cognitive ability in old age [35]. There is mounting evidence from the field of cognitive epidemiology showing that differences in prior cognitive ability are associated with health, morbidity and mortality outcomes, including those related to cerebrovascular disease [36,37]. It is possible that previously found cross-sectional associations between retinal vascular measures and cognitive ability are confounded by prior cognitive ability. Shalev et al conducted one of the few studies which reported an association between non-pathological cognitive ability and retinal vascular measures. They found that wider retinal venular calibre measured at age 38 years was significantly associated with poorer cognitive ability measured in childhood, and in adulthood [20]. However, they did not adjust for childhood cognitive ability in the association between retinal venular calibre and adulthood cognitive ability, and as a result, the degree to which retinal vascular differences independently accounted for variance in age 38 cognitive ability was unclear. If retinal vascular differences are related to normal cognitive function, it is possible that their contribution is small in relation to that of childhood cognitive ability. Patton and colleagues found childhood IQ to account for almost 20% of the variance in cognitive ability assessed in old age, whilst retinal parameters accounted for 3.7% at the most [19]. The present study is rare in having a valid measure of childhood cognitive ability, retinal imaging data, and a comprehensive set of cognitive ability measures from old age.

In this study we investigated the extent to which retinal vascular fractal dimension (as a possible marker of cerebral microvascular disease) contributes to differences in non-pathological cognitive ability in old age, independently of childhood mental ability.

Methods

Ethical permission for the Lothian Birth Cohort 1936 (LBC1936) study protocol was obtained from the Multi-Centre Research Ethics Committee for Scotland and from the Lothian Research Ethics Committee for Scotland. The research was carried out in compliance with the Helsinki Declaration. Written, informed consent was given by all participants.

LBC1936 Sample

Participants were a sub-sample of the LBC1936: a longitudinal study of cognitive ageing. This cohort comprises 1091 men and women, most of whom took part in the Scottish Mental Survey 1947 (SMS1947) [35,38]. Initial assessment took place between 2004 and 2007 when participants were about 70 years of age (M = 69.5, ± 0.8). The majority were living in the city of Edinburgh and surrounding Lothian area. A comprehensive description of recruitment and assessment procedures is available in an open-access protocol paper [39]. Data for the current study was mainly drawn from a second wave of the study (n = 866) [40]. Briefly, participants gave sociodemographic and medical history details during structured interviews, underwent repeat cognitive and physical testing, and completed a series of questionnaires including lifestyle and personality items, at about age 73 (M = 72.5, ± 0.7). Retinal photographs were taken at this time. Six hundred and sixty three participants had at least one image suitable for fractal analysis. Individuals with a Mini-Mental State Examination (MMSE) score < 24 were excluded (n = 6); this cut-off was used to exclude individuals with possible dementia. Participants with
images of substandard quality for fractal analysis were also excluded ($n = 9$). A total of 648 remained for statistical analyses (see Fig. 1).

Cognitive Ability

**Moray House Test No. 12.** The Moray House Test (MHT) No. 12 is a psychometric intelligence test which was validated at age 11 years against the Terman-Merrill revision of the Binet Scales [41,42]. It encompasses a range of items including reasoning, arithmetic, and
spatial items, has a time-limit of 45 minutes, and a maximum score of 76. Participants first sat the MHT on 4th June 1947 as part of the SMS1947, along with almost all schoolchildren in Scotland aged about 11 years. MHT scores were corrected for age in days at time of testing and converted to an IQ-type scale for the full LBC1936 sample (mean = 100, SD = 15). This will be referred to as age 11 IQ. Of the 648 participants included in the analyses, 605 participants had completed the MHT at age 11.

Cognitive Domains. A general cognitive ability factor \((g)\) was derived from principal components analysis (PCA) of six Wechsler Adult Intelligence Scale-III (WAIS-III) \([43]\) subtests: Symbol Search, Digit Symbol Coding, Matrix Reasoning, Letter-Number Sequencing, and Block Design. Likewise, a processing speed factor was derived from scores on a set of speed measures: Symbol Search and Digit Symbol Coding from WAIS-III; and also measures of Simple and Four-Choice Reaction Time \([44]\), and Inspection Time \([45]\). The same method was used to derive a memory factor from two WAIS-III subtests (Letter-Number Sequencing and Digit Span Backwards) and six Wechsler Memory Scale (WMS-III) subtests \([46]\): Logical Memory I Immediate Recall and II Delayed Recall, Spatial Span Forwards and Spatial Span Backwards, and Verbal Paired Associates I Immediate Recall and II Delayed Recall. The extraction of these factors was described previously \([47,48]\).

Additional Variables
Interview with a trained psychologist elicited self-reported presence or history of hypertension, cardiovascular disease, stroke, diabetes, and current smoking status (current smoker, ex-smoker, or non-smoker).

Retinal Image Analysis
Retinal images from both eyes were captured with a nonmydriatic camera at 45° FOV (CRDGi; Canon USA Inc., Lake Success, NY) and stored with 8 bits per colour plane, at 2048 x 3072 pixels and in TIFF format. Images were down-sampled to 685 x 584 pixels prior to processing and analysed by an expert retinal image analyst (TM) using custom software built in MATLAB (The MathWorks, Natwick, MA) \([49]\). Automatic segmentation of the retinal microvascular network (arterioles and venules) was performed using an algorithm described previously \([50]\) which classifies each pixel of a fundus image as vessel or non-vessel to produce a segmented map of the retinal vasculature (see Fig. 2). Prior to fractal analysis computationally segmented images were inspected and obvious artefacts, such as areas of low contrast noise or “ring” artefacts caused by dust on the camera, were corrected or removed. Fractal analysis may be more sensitive to changes in vascular patterns when skeletons rather than images containing vessel width information are considered \([51]\). Therefore all images were skeletonised by iterative deletion of pixels \([52]\). Finally, monofractal and multifractal analysis was applied.

In the monofractal approach a single \(D_f(D_{\text{box}})\) was measured using box-counting: the vessel map or skeletonized version was overlaid with a series of boxes of increasing size \(l\), and the number of boxes \(N\) containing at least one object pixel (representing part of the retinal vascular tree) was counted. The logarithm of \(N\) was plotted against the logarithm of \(l\). \(D_{\text{box}}\) was the slope of the best fit straight line of the plotted points \([53]\).

In the multifractal approach multiple fractal dimensions were measured at 1000 random points on the vessel maps and skeletonised images. The generalized sandbox method \([34]\) was used to investigate the effect of scale on the \(D_f\). Multifractal dimensions \(D_f\) for real \(f\) are a more versatile parameter in describing geometrical properties. Had the retinal vessel tree been a simple monofractal, the \(D_f\) would have been constant for all scales, \(f\). However, as expected the retinal tree displayed multifractal properties, giving different fractal dimensions as the scale was...
changed. We computed multifractal dimensions $D_0$, $D_1$, and $D_2$ as these have previously been reported as likely sensitive markers of small vascular changes [34]. $D_0$, $D_1$ and $D_2$ are commonly referred to as the capacity dimension, the entropy dimension and the correlation dimension, respectively. As we were unsure of the optimum one to use we investigated all three. Comparing the results enabled us to establish which was the most effective.

Implementation of this algorithm was trained and tested using a set of 20 images, manually segmented by 2 human observers as well as by the software. Fractal analysis of the manual segmentation performed by the ground truth observer was taken as the reference with which to compare fractal analysis of a second manual segmentation by a second observer and also the computational segmentation. A Bland-Altman approach [54] was used to assess the agreement between $D_f$ measurements, with mean differences and coefficients of repeatability (CR) computed. These are summarized in Table 1.

### Statistical Analysis

All analyses were conducted using SPSS version 21 (IBM, NY, USA). There were moderate to strong, but far from perfect, correlations between left and right eye fractal dimensions (Pearson coefficients between 0.403–0.582); therefore, we conducted analyses on left and right eyes separately. Retinal vascular parameters were analysed as continuous (per 1 SD increase). Cognitive domain and individual subtest scores were normally distributed; we therefore used multiple linear regression with cognitive domains and subtest scores as dependent variables, and the
retinal microvascular fractal dimensions as independent variables. Three models were fitted to the data with adjustments for potential confounding factors made in each. Age and sex were covariates in all three models. Age 11 IQ was included as an additional covariate in the second model. The third model adjusted for age, sex, age 11 IQ, hypertension, cardiovascular disease, diabetes, stroke, and current smoking status (non-smoker or ex-smoker vs. current smoker). A post hoc power analysis using pwr.r.test from the pwr package in R revealed that 648 subjects would provide 80% power to detect correlation coefficients of small effect size (.11; after Cohen) [55] with alpha set at .05, two-tailed.

### Results

The mean of the differences between fractal dimensions for two observers and between the first (ground truth) observer and the computation segmentation were very similar in magnitude, though the CR was slightly larger for computational segmentation evaluated against first observer (see Table 1). However, the results indicated that the computational segmentation was within an acceptable level of performance for the identification of vessels (i.e. it was similar to someone repeating manual segmentation) and so provided suitable input to fractal analysis.

The baseline characteristics for the cohort are summarized in Table 2. Of the 648 participants (326 men, 50.3%) included in the analyses, seven participants did not have a general (g) cognition score, 32 did not have a processing speed score, 27 did not have a memory score, and 120 did not have the full range of \( D_f \) measurements. Mean cognitive domain scores and retinal vascular \( D_f \) values are summarized in Table 3. Greater \( D_f \) represents greater complexity. Greater g, processing speed, and memory domain scores represent better performance. The cognitive domain scores reported are standardised variables (mean = 0, SD = 1) for the whole sample.

Table 4 presents the associations between retinal microvascular \( D_f \) and ability in the three cognitive domains. Three of the 24 tests conducted using the basic model were significant at the conventional p value of < .05. This is slightly more than one would expect by chance, but
no association would survive Bonferroni type correction for multiple statistical testing. Full Bonferroni correction would not be appropriate in this instance given that the retinal measures are not independent (Pearson coefficients between 0.708–0.982) and neither were the cognitive measures (Pearson coefficients between 0.438–0.735). In addition to this, no associations were verified by an equivalent association in the opposite eye, regardless of there being a moderate correlation between left and right eye measures.

The unadjusted significant associations were as follows. In the basic age- and sex- adjusted model right eye D1 was significantly associated with $g$ ($\beta = 0.10, P = 0.021$) and processing speed ($\beta = 0.10, P = 0.028$). Similarly, right eye D2 was significantly associated with $g$ ($\beta = 0.09,$ Table 2. Baseline Characteristics of Participants with Retinal Images of Sufficient and Insufficient Quality for Fractal Analysis.

| Characteristics                        | Gradable* (n = 648) | Ungradeable† (n = 9) |
|----------------------------------------|---------------------|----------------------|
| Age, years, mean (SD)                  | 72.4 (0.71)         | 72.4 (0.74)          |
| Male, n (%)                            | 326 (50.3)          | 6 (66.7)             |
| Age 11 IQ, mean (SD)                   | 102 (14.0)          | 108 (9.80)           |
| Hypertension, n (%)                    | 313 (48.3)          | 4 (44.4)             |
| Diabetes, n (%)                        | 61 (9.4)            | 0 (0)                |
| Current smoker, n (%)                  | 52 (8.0)            | 2 (22.2)             |
| Cardiovascular disease, mean (%)       | 177 (27.3)          | 1 (11.1)             |
| Stroke, n (%)                          | 39 (6.0)            | 0 (0)                |

* Participants with at least one retinal image of sufficient quality for fractal analysis
† Participants with retinal images of insufficient quality for fractal analysis

doi:10.1371/journal.pone.0121119.t002

Table 3. Descriptive Statistics of the Cognitive Domains and Fractal Dimensions of the Retinal Vascular Network.

| Cognitive Domain                  | n  | Mean | SD  | Range        |
|-----------------------------------|----|------|-----|--------------|
| General (g) Cognitive Ability     | 641| 0.04 | 0.99| -3.59–3.11   |
| Processing Speed                  | 616| 0.08 | 0.94| -3.18–2.75   |
| Memory                            | 621| 0.02 | 0.98| -3.82–2.21   |

Left Eye Fractal Dimension

| Dbox | 530 | 1.42 | 0.02 | 1.36–1.48 |
| D0   | 531 | 1.68 | 0.02 | 1.59–1.76 |
| D1   | 529 | 1.64 | 0.03 | 1.55–1.72 |
| D2   | 528 | 1.62 | 0.03 | 1.54–1.70 |

Right Eye Fractal Dimension

| Dbox | 537 | 1.43 | 0.02 | 1.35–1.50 |
| D0   | 538 | 1.68 | 0.02 | 1.60–1.77 |
| D1   | 539 | 1.65 | 0.03 | 1.57–1.75 |
| D2   | 538 | 1.63 | 0.03 | 1.55–1.73 |

Mean, standard deviation, and range of cognitive domain scores and retinal vascular fractal dimensions. $D_{\text{box}}$ = monofractal dimension $D_0, D_1, D_2 =$ multifractal dimension

N varies due to incomplete range of fractal dimension measurements and/or missing subtest data.

doi:10.1371/journal.pone.0121119.t003
There was also a statistical trend with right eye D0 ($\beta = 0.08, P = 0.063$; processing speed: $\beta = 0.07, P = 0.094$). No association was found between monofractal or multifractal retinal vascular Df and memory in this model. With the exception of a statistical trend between left eye Dbox and processing speed ($\beta = -0.08, P = 0.094$), no association was found between monofractal dimension Dbox and any cognitive domain.

IQ at age 11 was not associated with any of the retinal microvascular Df measures at age 73 (Left Dbox: $\beta = 0.007, P = 0.875$; Left D0: $\beta = 0.03, P = 0.491$; Left D1: $\beta = 0.000, P = 0.996$; Left D2: $\beta = -0.004, P = 0.931$; Right Dbox: $\beta = 0.01, P = 0.809$; Right D0: $\beta = 0.08, P = 0.063$; Right D1: $\beta = 0.07, P = 0.111$; Right D2: $\beta = 0.05, P = 0.236$). The addition of age 11 IQ as a covariate in model 2 weakened the associations between D0, D1, and D2 with g and processing speed, the $\beta$ coefficients were reduced by more than half in some cases, and in all cases significance was

### Table 4. Multiple Regression Models using Retinal Vascular Fractal Dimension to predict Ability in Three Cognitive Domains.

| Cognitive Domain, Fractal Dimension, & Laterality of Eye | Model 1 | Model 2 | Model 3 |
|---------------------------------------------------------|---------|---------|---------|
|                                                          | n       | $\beta$ | $P$     | n       | $\beta$ | $P$     | n       | $\beta$ | $P$     |
| g Dbox R                                                  | 532     | 0.04    | .322    | 502     | 0.03    | .353    | 502     | 0.04    | .250    |
|                                                         | 523     | -0.03   | .478    | 485     | -0.03   | .432    | 485     | -0.03   | .395    |
| D0 R                                                     | 533     | 0.08    | .063*   | 503     | 0.02    | .604    | 503     | 0.03    | .436    |
|                                                         | 524     | 0.000   | .995    | 486     | -0.01   | .900    | 486     | -0.01   | .825    |
| D1 R                                                     | 534     | 0.10    | .021*   | 503     | 0.03    | .404    | 503     | 0.04    | .324    |
|                                                         | 522     | 0.01    | .904    | 484     | 0.000   | .993    | 484     | -0.01   | .749    |
| D2 R                                                     | 533     | 0.09    | .035*   | 502     | 0.04    | .259    | 502     | 0.04    | .244    |
|                                                         | 521     | 0.001   | .976    | 483     | -0.01   | .812    | 483     | -0.02   | .608    |
| Speed Dbox R                                             | 512     | 0.04    | .385    | 484     | 0.03    | .447    | 484     | 0.04    | .315    |
|                                                         | 503     | -0.08   | .094†   | 467     | -0.06   | .195    | 467     | -0.05   | .257    |
| D0 R                                                     | 513     | 0.07    | .094†   | 485     | 0.04    | .341    | 485     | 0.05    | .250    |
|                                                         | 504     | -0.04   | .386    | 468     | -0.02   | .625    | 468     | -0.02   | .698    |
| D1 R                                                     | 514     | 0.10    | .028*   | 485     | 0.06    | .179    | 485     | 0.06    | .136    |
|                                                         | 502     | -0.04   | .429    | 466     | -0.03   | .473    | 466     | -0.03   | .452    |
| D2 R                                                     | 513     | 0.09    | .035*   | 484     | 0.07    | .115    | 484     | 0.07    | .092†   |
|                                                         | 502     | -0.03   | .583    | 466     | -0.03   | .506    | 466     | -0.03   | .466    |
| Memory Dbox R                                            | 513     | -0.03   | .539    | 485     | -0.02   | .673    | 485     | -0.01   | .811    |
|                                                         | 506     | 0.07    | .142    | 470     | -0.08   | .050*   | 470     | -0.08   | .040*   |
| D0 R                                                     | 514     | 0.02    | .719    | 486     | -0.02   | .545    | 486     | -0.02   | .611    |
|                                                         | 506     | -0.05   | .232    | 470     | -0.07   | .084†   | 470     | -0.07   | .069†   |
| D1 R                                                     | 515     | 0.02    | .734    | 486     | -0.03   | .421    | 486     | -0.03   | .466    |
|                                                         | 505     | -0.06   | .175    | 469     | -0.07   | .053†   | 469     | -0.08   | .038*   |
| D2 R                                                     | 514     | 0.000   | .992    | 485     | -0.03   | .419    | 485     | -0.03   | .439    |
|                                                         | 505     | -0.06   | .188    | 469     | -0.08   | .041*   | 469     | -0.08   | .029*   |

Data are presented as standardised beta coefficients reflecting change in cognitive domain score associated with an increase of 1 SD unit in fractal dimension. Model 1 adjusted for age and sex; Model 2 adjusted for age, sex, and age 11 IQ; Model 3 adjusted for age, sex, age 11 IQ, hypertension, diabetes, cardiovascular history, stroke, current smoking status.

Dbox = monofractal dimension; Do, D1, D2 = multifractal dimension.

N varies due to incomplete range of fractal dimension measurements and/or missing subtest data.

* Significant ($p < 0.05$).
† Trend ($p < 0.10$).

P = 0.035) and processing speed ($\beta = 0.09, P = 0.035$). There was also a statistical trend with right eye D0 ($g; \beta = 0.08, P = 0.063$; processing speed: $\beta = 0.07, P = 0.094$). No association was found between monofractal or multifractal retinal vascular Df and memory in this model. With the exception of a statistical trend between left eye Dbox and processing speed ($\beta = -0.08, P = 0.094$), no association was found between monofractal dimension Dbox and any cognitive domain.

IQ at age 11 was not associated with any of the retinal microvascular Df measures at age 73 (Left Dbox: $\beta = 0.007, P = 0.875$; Left D0: $\beta = 0.03, P = 0.491$; Left D1: $\beta = 0.000, P = 0.996$; Left D2: $\beta = -0.004, P = 0.931$; Right Dbox: $\beta = 0.01, P = 0.809$; Right D0: $\beta = 0.08, P = 0.063$; Right D1: $\beta = 0.07, P = 0.111$; Right D2: $\beta = 0.05, P = 0.236$). The addition of age 11 IQ as a covariate in model 2 weakened the associations between D0, D1, and D2 with g and processing speed, the $\beta$ coefficients were reduced by more than half in some cases, and in all cases significance was
lost. The further addition of all cardiovascular risk factors as covariates in model 3 did not alter these associations significantly, though there was a statistical trend between right eye \( D_2 \) and processing speed (\( \beta = 0.07, P = 0.092 \)). Accounting for age 11 IQ in the association between retinal \( D_1 \) and memory had the converse effect to that seen with the other domain scores. After adjustment for age 11 IQ, left eye \( D_1 \) analysed using monofractal and multifractal methods significantly predicted memory (\( D_{\text{box}}: \beta = -0.08, P = 0.050; D_2: \beta = -0.08, P = 0.041 \)), and there was a statistical trend with \( D_0 \) (\( \beta = -0.07, P = 0.084 \)) and \( D_1 \) (\( \beta = -0.07, P = 0.053 \)). Significance was maintained when all cardiovascular risk factors were accounted for in model 3 (\( D_{\text{box}}: \beta = -0.08, P = 0.040; D_1: B = -0.08, P < 0.038; D_2: \beta = -0.08, P = 0.029 \)), again there was a statistical trend with \( D_0 \) (\( \beta = -0.07, P = 0.069 \)).

The reversed direction of association indicates that increased branching complexity predicted poorer memory performance. However, again these associations were not corroborated by an equivalent finding when right eye retinal measures were tested and are therefore unlikely to be meaningful. Taken together, our results show no evidence that differences in retinal vascular fractal dimension contribute to cognitive ability in old age. We suggest that in our sample, differences in childhood ability, but not retinal vascular parameters, account for much of the variance in cognitive ability in later life.

SI Table contains results from the analysis of individual cognitive subtests.

Discussion

Microvascular disease is a major contributor to cognitive dysfunction in individuals with and without dementia. However, its role in non-pathologic cognitive function is unclear. The present study investigated cross-sectional associations between retinal vascular \( D_0 \), a putative marker of cerebral microvascular health, and three domains of cognitive ability in a sample of older adults without cognitive impairment. After adjustment for childhood IQ and traditional cardiovascular risk factors, greater left eye monofractal and multifractal dimensions (\( D_{\text{box}}, D_1, \) and \( D_2 \)) were associated with poorer memory performance, however, neither left nor right eye fractal dimensions were associated with \( g \) or processing speed, and no association was verified by an equivalent result in the contralateral eye.

The data on retinal microvascular topography and non-pathological cognitive ageing have been limited, and direct comparison with previous studies is not possible due to various methodological differences in the research to date. The Lothian Birth Cohort 1921 (LBC1921) study examined the associations between quantitative measures of suboptimal retinal vascular branching geometry and cognitive ability in 321 men and women aged either 83 or 84. After adjusting for childhood IQ, cardiovascular risk factors, and socio-demographic variables, deviation from the optimal retinal vascular bifurcation angle accounted for 2.6% of the variance in logical memory test scores of older adults, while deviation from the optimal retinal vascular branching coefficient accounted for 3.4% of the variance in a general cognitive ability (\( g \)) score, and 3.7% in verbal fluency test score. Similar results were found in sample of 1007 men and women from the Dunedin Multidisciplinary Health and Development study, a population based cohort followed from birth. In this study, wider venular calibre was associated with lower total and delayed Rey auditory verbal learning scores, lower scores on several tests of executive function, and lower scores on all components of WAIS-IV. Our study results differ from these data in that no association was found between retinal vascular \( D_1 \) and measures of \( g \) or processing speed, and retinal vascular \( D_1 \) was only weakly associated with memory, though this was not confirmed by the contralateral eye and therefore unlikely to be meaningful. Some of this difference may be attributable to the differences in mean age of the cohorts. The LBC1921 cohort was aged between 83 and 84 years old, an age at which between-person
variability in cognitive ability scores and retinal vascular state may be increased; however, frac-
tal dimension was not measured in the LBC1921 study, and it is not possible to say if cognitive
ability would have been associated with retinal vascular $D_f$ in that sample. The Dunedin study
cohort had a mean age of 38, and their results may be more consistent with the hypothesis that
cognitive impairment is more greatly influenced by cerebral microvascular disease in younger
compared to older adults [18]. Though, it is unlikely that much disease would be present in
people of this age.

Qualitative measures of retinal vascular abnormality have also been associated with cogni-
tive ability in older age. Results from the population-based Atherosclerosis Risk in Commu-
nities (ARIC) study showed that in a sample of 8734 persons, individuals with any retinopathy,
microaneurysm, retinal haemorrhage or soft exudates, were 2.6 to 3.39 times more likely to
score below mean on the delayed word recall test than those without [17]. Wong and colleagues
also found an association between presence of retinopathy and low scores on the digit symbol
substitution test, in both the ARIC study and in another sample of 2211 participants from the
population-based Cardiovascular Health Study (CHS) In contrast to quantitative measures de-
signed to identify subtle changes to the vasculature, qualitative measures are indicative of more
severe states and even diseases of the retinal microvasculature, which are often associated with
the breakdown of the blood-brain barrier. This difference in severity of retinal vascular pathol-
ogy may partly explain why associations between cognitive ability and qualitative measures
have been more consistent than those assessing less severe changes, such as narrowing of the
vessels [18].

The relationship between ‘normal’ cognitive ageing and retinal vascular fractal dimension
has not previously been investigated. The optimal retinal vascular $D_f$ is said to be 1.7, and devi-
ations from this have previously been associated with ageing [33], diabetic retinopathy [25]
and death resulting from coronary heart disease (CHD) [26]. Cheung and colleagues recently
found a significant association between reduced retinal vascular $D_f$ and cognitive dysfunction.
Individuals with the lowest $D_f$ were between 1.03 and 2.82 times more likely to have cognitive
dysfunction [22]. In a separate study the same authors found, that for every 1 SD unit decrease
in $D_f$, the likelihood of having Alzheimer’s Disease rose by 1.54 [23].

This study has several strengths. It makes a novel contribution to research investigating the
relationship between parameters of the retinal microvasculature and cognitive function. To our
knowledge, it is the first to examine the relationship between retinal vascular fractal dimension
and non-pathologic cognitive ability, and the only one to do so using both monofractal and
multifractal methods of analysis. It is important to note that generalized dimension spectrums
for each image analysed, showed that the retinal vessel structures were all geometrical multi-
fractals. Second, we were able to make statistical adjustment for childhood cognitive ability, a
factor known to account for a large proportion of variance in later life cognitive ability [35, 56].
Third, cognitive domain scores were based on a broad range of neuropsychological tests, giving
a robust measure of general (g) cognitive ability, processing speed, and memory. Finally, in
contrast to previous studies [32,33] by analysing left and right eye retinal measures separately
we were able to show that no association was substantiated by the same result using measure-
ments from the contralateral eye (see S1–S3 Figs).

Limitations of the study should also be noted. Problems exist with the automated segmenta-
tion algorithm: the edge of the optic disk is sometimes wrongly detected as a vessel, incorrect
detections result from the underlying choroidals, gaps appear in the middle of vessels if the
central light reflex is bright, some vessel paths are broken due to poor image contrast and very
small vessels are sometimes missed. All of these issues lead to a reduction in segmentation ac-
curacy and fractal dimension of the retinal vasculature. Irrespectively, our images have very
good agreement between the segmentations by two observers and so for fractal analysis the
mean differences and CRs were small (see Table 1). When comparing fractal dimensions for 
computerised segmentations and ground truth (first human segmentation), mean differences 
were also small and CRs were an acceptable level. These results show that for a reasonable 
image quality, repeatability of fractal analysis performed on computerised segmentations is 
close to the repeatability found when two observers independently perform manual tracing.
For large epidemiological studies, i.e. greater than fifty images, this would be at acceptable level in order to detect small changes.

Second, adjustment was not made for myopic refractive errors. Increasing myopia is associ- 
ated with reduced retinal vascular fractal dimension, though this reduction is likely to be minimal except in cases of high myopia [57]. Additionally, myopia is less prevalent in older individuals, and therefore in the LBC participants myopia may not affect results to the same extent as a younger sample [58]. Differences in retinal vascular fractal dimension have also been found when comparing images from normal eyes to those from individuals diagnosed with diabetic retinopathy [25, 32]. Though presence of diabetes was not part of the exclusion criteria for the present study, no single image judged as ungradeable belonged to a diabetic individual, and adjustment for the presence of diabetes was made in the analyses. Third, the LBC1936 is a self-selecting sample, and as such it is likely to be healthier and more cognitively able than the general population [56]. It should be noted however, that though retinal vascular $D_f$ does not appear to be associated with cognitive function in this sample at age 73, associations may be found as the sample ages and vascular pathology progresses. And though an association with cognitive ability was not found in this study, that is not to say that individual differences in retinal vascular $D_f$ are not indicative of abnormality and disease of small vessels in general. Small vessel disease is a systemic disorder [2], and though small vessels of the brain may bear the burden of this disease in some individuals, organs through the body will be most affected [4]. Further research is required to understand the full potential of fractal analysis as an early indicator of disease in the brain and body. Finally, retinal images were taken during only one wave of testing, restricting us to cross-sectional analyses. Access to retinal images taken at multiple time points would allow examination of these associations in relation to longitudinal change.

**Conclusion**

Three out of the 24 comparisons were found to be significant. Although this is more than one would expect by chance, no association would survive Bonferroni correction for multiple statistical testing. Significant unadjusted associations were weakened and lost significance after co- 
varying for IQ at age 11 and cardiovascular risk factors, and not one association was verified by an equivalent finding using measurements from the contralateral eye. We cautiously suggest that our results do not reject the null hypothesis, that differences in retinal vascular $D_f$ are not associated with cognitive ability in old age. Further research is required to elucidate the relationship between parameters of the retinal microvascular network and non-pathological cognitive function.

**Supporting Information**

S1 Fig. Change in cognitive domain score associated with 1 SD unit increase in fractal di- 

S2 Fig. Change in cognitive subtest score associated with 1 SD increase in right eye fractal di- 

PDF

PDF
significant at ± 0.08 (p < 0.05). 1: Symbol search, 2: digit symbol coding, 3: matrix reasoning, 4: letter–number sequencing, 5: digit span backwards, 6: block design, 7: simple reaction time, 8: 4-choice reaction time, 9: inspection time, 10: spatial span forwards, 11: spatial span backwards, 12: verbal paired associates immediate recall, 13: verbal paired associates delayed recall, 14: logical memory immediate recall, 15: logical memory delayed recall.

S3 Fig. Change in cognitive subtest score associated with 1 SD increase in left eye fractal dimension. Dbox = monofractal dimension. D0, D1, D2 = multifractal dimension. β significant at ± 0.08 (p < 0.05). 1: Symbol search, 2: digit symbol coding, 3: matrix reasoning, 4: letter–number sequencing, 5: digit span backwards, 6: block design, 7: simple reaction time, 8: 4-choice reaction time, 9: inspection time, 10: spatial span forwards, 11: spatial span backwards, 12: verbal paired associates immediate recall, 13: verbal paired associates delayed recall, 14: logical memory immediate recall, 15: logical memory delayed recall.

S1 Table. Multiple Regression Models Using Retinal Vascular Fractal Dimension to predict Ability in Cognitive Subtests. Note. * p < 0.05; † trend p < 0.10. Dbox = monofractal dimension; D0, D1, D2 = multifractal dimension; VPA = verbal paired associates; LM = logical memory. Standardised beta coefficients reflect change in cognitive subtest score associated with an increase of 1 SD unit in fractal dimension. Model 1 adjusted for age and sex; Model 2 adjusted for age, sex, and age 11 IQ; Model 3 adjusted for age, sex, age 11 IQ, hypertension, diabetes, cardiovascular history, stroke, current smoking status. N varies due to incomplete range of fractal dimension measurements and/or missing subtest data.

Acknowledgments
We thank the Scottish Council for Research in Education for allowing access to the SMS1947. We thank the LBC1936 Study participants who contributed to these studies, the research staff responsible for data collection, and staff at the Wellcome Trust Clinical Research Facility. JMS and IJD are members of The University of Edinburgh Centre for Cognitive Ageing and Cognitive Epidemiology, part of the cross council Lifelong Health and Wellbeing Initiative.

Author Contributions
Conceived and designed the experiments: IJD AMT TJM. Performed the experiments: RDH LI. Analyzed the data: IJD AMT TJM. Contributed reagents/materials/analysis tools: TJM. Wrote the paper: AMT TJM RDH LI BD JMS IJD. Directed cohort: IJD.

References
1. O’Brien JT, Erkinjuntti T, Reisberg B, Roman G, Sawada T, Pantoni L, et al. Vascular cognitive impairment. Lancet Neurol. 2003; 2: 89–98. PMID: 12849265
2. Thompson CS, Hakim AM. Living beyond our physiological means: small vessel disease of the brain is an expression of a systemic failure in arteriolar function: a unifying hypothesis. Stroke. 2008; 40: e322–e330. doi: 10.1161/STROKEAHA.108.542266 PMID: 19228835
3. Knopman DS. Cerebrovascular disease and dementia. Br J Radiol. 2007; 80: S121–S127. doi: 10.1259/bjr/75681080 PMID: 18445742
4. Pantoni L. Cerebral small vessel disease: from pathogenesis and clinical characteristics to therapeutic challenges. Lancet Neurol. 2010; 9: 669–701. doi: 10.1016/S1474-4422(10)70104-6 PMID: 20610345
5. Patton N, Aslam T, MacGillivray T, Pattie A, Deary IJ, Dhillon B. Retinal vascular image analysis as a potential screening tool for cerebrovascular disease: a rationale based on homology between cerebral and retinal microvascularatures. J Anat. 2005; 206: 319–348. PMID: 15817102

6. Murray CD. The physiological principle of minimum work: I. The vascular system and the cost of blood volume. Proc Natl Acad Sci U S A. 1926; 12: 207–214. PMID: 16576980

7. Zamir M. Fractal dimensions and multifractality in vascular branching. J Theor Biol. 2001; 212: 183–190. PMID: 11531384

8. Patton N, Aslam TM, MacGillivray T, Deary IJ, Dhillon B, Eikelboom RH, et al. Retinal image analysis: concepts, applications and potential. Prog Retin Eye Res. 2006; 25: 99–127. PMID: 16154379

9. Ikram MK, de Jong FJ, Vingerling JR, Witterman JC, Hofman A, Breitler M, et al. Are retinal arteriolar or venular diameters associated with markers for cardiovascular disorders? The Rotterdam Study. Invest Ophthalmol Vis Sci. 2004; 45: 2129–2134. PMID: 15227386

10. Wong TY, Hubbard LD, Klein R, Marino EK, Kronmal R, Sharrett AR, et al. Retinal microvascular abnormalities and blood pressure in older people: the Cardiovascular Healthy Study. Br J Ophthalmol. 2002; 86: 1007–1013. PMID: 12185128

11. Klein R, Klein BE, Moss SE, Wong TY, Hubbard L, Cruickshanks KJ, et al. Retinal vascular abnormalities in persons with type 1 diabetes the Wisconsin Epidemiologic Study of Diabetic Retinopathy: XVIII. Ophthalmology. 2003; 110: 2118–2125. PMID: 14597518

12. Qiu C, Cotch MF, Sigurdsson S. Cerebral microbleeds, retinopathy, and dementia: the AGES-Reykjavik Study. Neurology. 2010; 75: 2221–2228. doi: 10.1212/01.wnl.0000381347.10899.f5 PMID: 21172845

13. Longstreth WT, Larsen EK, Klein R, Wong TY, Sharrett AR, Lefkowitz D, et al. Associations between findings on cranial magnetic resonance imaging and retinal photography in the elderly: the Cardiovascular Health Study. Am J Epidemiol. 2007; 165: 78–84. PMID: 17041135

14. Kwa VI, van der Sande JJ, Stam J, Tijmes N, Vrooland JL. Retinal arterial changes correlate with cerebrovascular disease. Neurology. 2002; 59: 1536–1540. PMID: 12451193

15. Cooper LS, Wong TY, Klein R, Sharrett AR, Bryan N, Hubbard LD, et al. Retinal microvascular abnormalities and MRI-defined subclinical cerebral infarction: the Atherosclerosis Risk in Communities Study. Stroke. 2006; 37: 82–86. PMID: 16306463

16. Cheung N, Mosley T, Islam A. Retinal microvascular abnormalities and subclinical magnetic resonance imaging brain infarct: a prospective study. Brain. 2010; 133: 1987–1993. doi: 10.1093/brain/awq127 PMID: 20519327

17. Wong TY, Klein R, Sharrett AR, Nieto J, Boland LL, Couper DJ, et al. Retinal microvascular abnormalities and cognitive impairment in middle-aged persons: The Atherosclerosis Risk in Communities Study. Stroke. 2002; 33: 1487–1492. PMID: 12052979

18. Baker ML, Marino Larsen EK, Kuller LH, Klein R, Klein BE, Siscovick DS, et al. Retinal microvascular signs, cognitive function, and dementia in older persons: the Cardiovascular Health Study. Stroke. 2007; 38: 2041–2047. PMID: 17525385

19. Patton N, Pattie A, MacGillivray T, Aslam T, Dhillon B, Gow A, et al. The association between retinal vascular network geometry and cognitive ability in an elderly population. Invest Ophthalmol Vis Sci. 2007; 48: 1995–2000. PMID: 17460252

20. Shaley I, Moffitt TE, Wong TY, Meier MH, Houts RM, Ding J, et al. Retinal vessel caliber and lifelong neuropsychological functioning: retinal imaging as an investigative tool for cognitive epidemiology. Psych Sci. 2013; 24: 1198–1207. doi: 10.1177/0956797612470959 PMID: 23678508

21. Liew G, Mitchell P, Wong TY, Lindley RI, Cheung N, Kaushik S, et al. Retinal microvascular signs and cognitive impairment. J Am Geriatr Soc. 2009; 57: 1892–1896. doi: 10.1111/j.1532-5415.2009.02459.x PMID: 19737331

22. Cheung CY, Ong SY, Ikram MK, Ong YT, Chen CP, Venketasubramanian N, et al. Retinal vascular fractal dimension is associated with cognitive dysfunction. J Stroke Cerebrovasc Dis. 2012; 21: 43–50. doi: 10.1016/j.jstrokecerebrovasdis.2012.09.002 PMID: 23099042

23. Cheung CY, Ong YT, Ikram MK, Ong SY, Li X, Hilal S, et al. Microvascular network alterations in the retina of patients with Alzheimer’s disease. Alzheimers Dement. 2013; 10: 135–142.

24. Ding J, Patton N, Deary IJ, Strachan MW, Fowkes FG, Mitchell RJ, et al. Retinal microvascular abnormalities and cognitive dysfunction: a systematic review. Br J Ophthalmol. 2008; 92: 1017–1025. doi: 10.1136/bjo.2008.141994 PMID: 18614569

25. Avakian A, Kalina RE, Sage EH, Rambhia AH, Elliott KE, Chuang EL, et al. Fractal analysis of region-based vascular change in the normal and non-proliferative diabetic retina. Curr Eye Res. 2002; 24: 274–280. PMID: 12324866
26. Liew G, Mitchell P, Rochtchina E, Wong TY, Hsu W, Lee ML, et al. Fractal analysis of retinal microvasculature and coronary heart disease mortality. Eur Heart J. 2011; 32: 422–429. doi: 10.1093/eurheartj/ehq431 PMID: 21138936

27. Masters BR. Fractal analysis of the vascular tree in the human retina. Annu Rev Biomed Eng. 2004; 6: 427–452. PMID: 15255776

28. Daxer A. Characterisation of the neovascularisation process in diabetic retinopathy by means of fractal geometry: diagnostic implications. Graefes Arch Clin Exp Ophthalmol. 1993; 231: 681–686. PMID: 8299974

29. Mainster MA. The fractal properties of retinal vessels: embryological and clinical implications. Eye (Lond). 1990; 4: 235–241.

30. Landini G, Murray PI, Misson GP. Local connected fractal dimensions and lacunarity analyses of 60° fluorescein angiograms. Invest Ophthalmol Vis Sci. 1995; 36: 2749–2755. PMID: 7499097

31. Doubal FN, MacGillivray TJ, Patton N, Dhillon B, Dennis MS, Wardlaw JM. Fractal analysis of retinal vessels suggests that a distinct vasculopathy causes lacunar stroke. Neurology. 2010; 74: 1102–1107. doi: 10.1212/WNL.0b013e3181d7dbb4 PMID: 20368631

32. Cheung N, Donaghue KC, Liew G, Rogers SL, Wang JJ, Lim S, et al. Quantitative assessment of early diabetic retinopathy using fractal analysis. Diabetes Care. 2009; 32: 106–110. doi: 10.2337/dc08-1233 PMID: 18835945

33. Azemin MZ, Kumar DK, Wong TY, Wang JJ, Mitchell P, Kawasaki R, et al. Age-related rarefaction in the fractal dimension of retinal vessel. Neurobiol Aging. 2012; 33: 194.e1–194.e4.

34. Stosić T & Stosić BD. Multifractal analysis of human retinal vessels. IEEE Trans Med Imaging. 2006; 25: 1101–1107. PMID: 16895002

35. Deary IJ, Whiteman MC, Starr JM, Whalley LJ, Fox HC. The impact of childhood intelligence on later life: following up the Scottish Mental Surveys of 1932 and 1947. J Pers Soc Psychol. 2004; 86: 130–147. PMID: 14717632

36. Gottfredson L, Deary IJ. Intelligence predicts health and longevity, but why? Curr Dir Psychol Sci. 2004; 13: 1–4. PMID: 18144600

37. Deary IJ, Weiss A, Batty GD. Intelligence and personality as predictors of illness and death: how researchers in differential psychology and chronic disease epidemiology are collaborating to understand and address health inequalities. Psychol Sci Public Interest. 2010; 11: 53–79.

38. Deary IJ, Whalley LJ, Starr JM. A lifetime of Intelligence: Follow-up Studies of the Scottish Mental Surveys of 1932 and 1947. Washington, DC: American Psychological Association; 2009.

39. Deary IJ, Gow AJ, Taylor MD, Corley J, Brett C, Wilson V, et al. The Lothian birth cohort 1936: a study to examine influences on cognitive ageing from age 11 to age 70 and beyond. BMC Geriatr. 2007; 7: 28. PMID: 18053258

40. Deary IJ, Gow AJ, Pattie A, Starr JM. Cohort profile: the Lothian Birth Cohorts of 1921 and 1936. Int J Epidemiol. 2012; 41: 1576–1584. doi: 10.1093/ije/dyr197 PMID: 22253310

41. Scottish Council for Research in Education (SCRE). The intelligence of Scottish Children: A National Survey of an Age Group. London, UK: University of London Press; 1933.

42. Scottish Council for Research in Education (SCRE). The Trend of Scottish Intelligence: A Comparison of the 1947 and 1932 Surveys of the Intelligence of Eleven-Year-Old Pupils. London, UK: University of London Press; 1949.

43. Wechsler D. WAIS-III UK Administration and Scoring Manual. London, UK: Psychological Corporation; 1998.

44. Deary IJ, Der G, Ford G. Reaction times and intelligence differences: a population-based cohort study. Intelligence. 2001; 29: 389–399.

45. Deary IJ, Simonotto E, Meyer M, Marshall A, Marshall I, Goddard N, et al. The functional anatomy of inspection time: an event-related fMRI study. Neuroimage. 2004; 22: 1466–1479. PMID: 15275904

46. Wechsler D. WMS-III UK Administration and Scoring Manual. London, UK: Psychological Corporation; 1998.

47. Luciano M, Gow AJ, Harris SE, Hayward C, Allerhand M, Starr JM, et al. Cognitive ability at age 11 and 70 years, information processing speed, and APOE variation: the Lothian Birth Cohort 1936 study. Psychol Aging. 2009; 24: 129–138. doi: 10.1037/a0014780 PMID: 19290744

48. Corley J, Gow AJ, Starr JM, Deary IJ. Is body mass index in old age related to cognitive abilities? The Lothian Birth Cohort 1936 Study. Psychol Aging. 2010; 25: 867–875. doi: 10.1037/a0020301 PMID: 21186916
49. MacGillivray TJ, Perez-Rovira A, Trucco E, Chin KS, Giachetti A, Lupascu C, et al. VAMPIRE: Vessel Assessment and Measurement Platform for Images of the Retina. In: Ng EYK, Tan JH, Acharya UR, Suri JS, editors. Human Eye Imaging and Modeling. Boca Raton, FL: CRC Press. 2012. pp. 23–38.

50. Soares JVB, Leandro JGG, Cesar RM, Jelinek HF, Cree MJ. Retinal vessel segmentation using the 2-D Gabor wavelet and supervised classification. IEEE Trans Med Imaging. 2006; 25: 1214–1222. PMID: 16967806

51. Parsons-Wingerter P, Elliot KE, Clark JI, Farr AG. Fibroblast growth factor-2 selectively stimulates angiogenesis of small vessels in arterial tree. Arterioscler Thromb Vasc Biol. 2000; 20: 1250–1256. PMID: 10807740

52. Lam L, Lee S, Suen CY. Thinning-methodologies—a comprehensive survey. IEEE Trans Pattern Anal Mach Intell. 1992; 14: 869–885.

53. MacGillivray TJ, Patton N, Doulal FN, Graham C, Wardlaw JM. Fractal analysis of the retinal vascular network in fundus image. Conf Proc IEEE Eng Med Biol Soc. 2007: 6456–6459. PMID: 18003503

54. Bland JM & Altman DJ. Statistical methods for assessing agreement between two methods of clinical measurement. Lancet. 1986; 1: 307–310. PMID: 2868172

55. Cohen J. A power primer. Psychol Bull. 1992; 112: 155–159. PMID: 19565683

56. Gow AJ, Johnson W, Patte A, Brett CE, Roberts B, Starr JM, et al. Stability and change in intelligence from age 11 to ages 70, 79, and 87: the lothian birth cohorts of 1921 and 1936. Psychol Aging. 2011; 26: 232–240. doi: 10.1037/a0021072 PMID: 20973608

57. Li H, Mitchell P, Liew G, Rochtchina E, Kifley A, Wong TY, et al. Lens opacity and refractive influences on the measurement of retinal vascular fractal dimension. Acta Ophthalmol. 2010; 88: e234–e240. doi: 10.1111/j.1755-3768.2010.01975.x PMID: 20662797

58. Wensor M. Prevalence and risk factors of myopia in Victoria, Australia. Arch Ophthalmol. 1999; 117: 658–663. PMID: 9339965