Physical nature of volume plasmon polaritons in hyperbolic metamaterials

Zhukovsky, Sergei; Kidwai, Omar; Sipe, J. E.

Published in:
Optics Express

Link to article, DOI:
10.1364/OE.21.014982

Publication date:
2013

Document Version
Publisher's PDF, also known as Version of record

Link back to DTU Orbit

Citation (APA):
Zhukovsky, S., Kidwai, O., & Sipe, J. E. (2013). Physical nature of volume plasmon polaritons in hyperbolic metamaterials. Optics Express, 21(12), 14982-14987. https://doi.org/10.1364/OE.21.014982

General rights
Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

• Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
• You may not further distribute the material or use it for any profit-making activity or commercial gain
• You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.
Physical nature of volume plasmon polaritons in hyperbolic metamaterials

Sergei V. Zhukovsky,1,2 Omar Kidwai,1 and J. E. Sipe1,*

1Department of Physics and Institute for Optical Sciences, University of Toronto, 60 St. George Street, Toronto, Ontario M5S 1A7, Canada
2DTU Fotonik – Department of Photonics Engineering, Technical University of Denmark, Ørsteds Pl. 343, DK-2800 Kongens Lyngby, Denmark

* sipe@physics.utoronto.ca

Abstract: We investigate electromagnetic wave propagation in multilayered metal-dielectric hyperbolic metamaterials (HMMs). We demonstrate that high-k propagating waves in HMMs are volume plasmon polaritons. The volume plasmon polariton band is formed by coupling of short-range surface plasmon polariton excitations in the individual metal layers.

© 2013 Optical Society of America

OCIS codes: (160.3918) Metamaterials; (160.1190) Anisotropic optical materials.

References and links

1. M. A. Noginov, Yu. A. Barnakov, G. Zhu, T. Tumkur, H. Li, and E. E. Narimanov, “Bulk photonic metamaterial with hyperbolic dispersion,” Appl. Phys. Lett. 94(15), 151105 (2009).
2. M. A. Noginov, H. Li, Yu. A. Barnakov, D. Dryden, G. Nataraj, G. Zhu, C. E. Bonner, M. Mayy, Z. Jacob, and E. E. Narimanov, “Controlling spontaneous emission with metamaterials,” Opt. Lett. 35(11), 1863–1865 (2010).
3. A. Reyes-Coronado, M. F. Acosta, R. I. Merino, V. M. Orera, G. Genanakis, N. Katsarakis, M. Kafesaki, Ch. Mavridis, J. García de Abajo, E. N. Economou, and C. M. Soukoulis, “Self-organization approach for THz polaritonic metamaterials,” Opt. Express 20(13), 14663–14682 (2012).
4. S. Foteinopoulou, M. Kafesaki, E. N. Economou, and C. M. Soukoulis, “Two-dimensional polaritonic photonic crystals as terahertz uniaxial metamaterials,” Phys. Rev. B 84(3), 035128 (2011).
5. Z. Jacob, J.-Y. Kim, G. V. Naik, A. Boltasseva, E. E. Narimanov, and V. M. Shalaev, “Engineering the photonic density of states with metamaterials,” Appl. Phys. B 100(1), 215–218 (2010).
6. Z. Jacob, I. I. Smolyaninov, and E. E. Narimanov, “Broadband Purcell effect: Radiative decay engineering with metamaterials,” Appl. Phys. Lett. 100(18), 181105 (2012).
7. D. R. Smith, D. Schurig, J. J. Mock, P. Kolinka, and P. Rye, “Partial focusing of radiation by a slab of indefinite media,” Appl. Phys. Lett. 84(13), 2244–2246 (2004).
8. Z. Jacob, L. V. Alekseyev, and E. Narimanov, “Optical Hyperlens: Far-field imaging beyond the diffraction limit,” Opt. Express 14(18), 8247–8256 (2006).
9. A. N. Podobubry, P. A. Belov, and Yu. S. Kivshar, “Spontaneous radiation of a finite-size dipole emitter in hyperbolic media,” Phys. Rev. A 84(2), 023807 (2011).
10. C. L. Cortes, W. Newman, S. Molesky, and Z. Jacob, “Quantum nanophotonics using hyperbolic metamaterials,” J. Opt. 14(6), 063001 (2012).
11. E. E. Narimanov and I. I. Smolyaninov, “Beyond Stefan-Boltzmann law: thermal hyper-conductivity,” arXiv:1109.5444 (2011).
12. I. I. Smolyaninov and E. E. Narimanov, “Metric signature transitions in optical metamaterials,” Phys. Rev. Lett. 105(6), 067402 (2010).
13. A. A. Basharin, M. Kafesaki, E. N. Economou, and C. M. Soukoulis, “Backward wave radiation from negative permittivity waveguides and its use for THz subwavelength imaging,” Opt. Express 20(12), 12752–12760 (2012).
14. B. Wood, J. B. Pendry, and D. P. Tsai, “Directed subwavelength imaging using a layered metal-dielectric system,” Phys. Rev. B 74(11), 115116 (2006).
15. A. Fang, T. Koschny, and C. M. Soukoulis, “Optical anisotropic metamaterials: Negative refraction and focusing,” Phys. Rev. B 79, 245127 (2009).
16. S. Ramakrishna, J. Pendry, M. Wiltshire, and W. Stewart, “Imaging the near field,” J. Mod. Opt. 50, 1419 (2003).
17. E. Narimanov, M. A. Noginov, H. Li, and Y. Barnakov, “Darker than Black: Radiation-absorbing Metamaterial,” in Quantum Electronics and Laser Science Conference, OSA Technical Digest (CD) (Optical Society of America, 2010), paper QPD4A.

18. P. G. Etcheogoin, E. C. Le Ru, and M. Meyer, “An analytic model for the optical properties of gold,” J. Chem. Phys. 125(16), 164705 (2006).

19. T. S. Eriksson, A. Hjortsberg, G. A. Niklasson, and C. G. Granqvist, “Infrared optical properties of evaporated alumina films,” Appl. Opt. 20(15), 2742–2746 (1981).

20. A. Chebykin, A. Orlov, A. Voizanova, S. Maslovski, Yu. Kivshar, and P. Belov, “Nonlocal effective medium model for multilayered metal-dielectric metamaterials,” Phys. Rev. B 84(11), 115438 (2011).

21. A. A. Orlov, P. M. Voroshilov, P. A. Belov, and Yu. S. Kivshar, “Engineered optical nonlocality in nanostructured metamaterials,” Phys. Rev. B 84(4), 045424 (2011).

22. O. Kidwai, S. V. Zhukovsky, and J. E. Sipe, “Dipole radiation near hyperbolic metamaterials: applicability of effective-medium approximation,” Opt. Lett. 36(13), 2530–2532 (2011).

23. I. Iorsh, A. Podlebsky, A. Orlov, P. Belov, and Yu. Kivshar, “Spontaneous emission enhancement in metal-dielectric metamaterials,” Phys. Lett. A 376(3), 185–187 (2012).

24. O. Kidwai, S. V. Zhukovsky, and J. E. Sipe, “Effective-medium approach to planar multilayer hyperbolic metamaterials: Strengths and limitations,” Phys. Rev. A 85(5), 053842 (2012).

25. X. Ni, S. Ishii, M. D. Thoreson, V. M. Shalaev, S. Han, S. Lee, and A. V. Kildishev, “Loss-compensated and active hyperbolic metamaterials,” Opt. Express 19(25), 25242–25254 (2011).

26. J. Schilling, “Uniaxial metallo-dielectric metamaterials with scalar positive permeability,” Phys. Rev. E 74(4), 046618 (2006).

27. I. Avrutsky, I. Salakhutdinov, J. Elser, and V. Podolskiy, “Highly confined optical modes in nanoscale metal-dielectric multilayers,” Phys. Rev. B 75(24), 241402(R) (2007).

28. S. Ishii, A. V. Kildishev, E. Narimanov, V. M. Shalaev, and V. P. Drachev, “Sub-wavelength interference pattern from volume plasmon polaritons in a hyperbolic medium,” Laser Photon. Rev. 7(2), 265–271 (2013).

29. E. Colak, H. Caglayan, A. O. Cakmak, A. D. Villa, F. Capolino, and E. Ozbay, “Frequency dependent steering with backward leaky waves via photonic crystal interface layer,” Opt. Express 17(12), 9879–9890 (2009).

30. H. Liu and K. J. Webb, “Leaky wave radiation from planar anisotropic metamaterial slabs,” Phys. Rev. B 81(20), 214104 (2010).

31. R. Ruppin, “Surface polaritons of a left-handed material slab,” J. Phys.: Condens. Matter 13(9), 1811 (2001).

32. S. Feng, J. M. Elson, and P. L. Overfelt, “Optical properties of multilayer metal-dielectric nanofilms with all-evanescent modes,” Opt. Express 13(11), 4113–4124 (2005).

33. G. Rosenblatt and M. Orenstein, “Competing coupled gaps and slabs for plasmonic metamaterial analysis,” Opt. Express 19(21), 20372–20385 (2011).

34. A. Yariv and P. Yeh, Optical Waves in Crystals (New York: Wiley, 1983).

35. T. Truong, J. Maria, J. Yao, M. Stewart, T. Lee, S. Gray, R. Nuzzo, and J. Rogers, “Nanopost plasmonic crystals,” Nanotechnol. 20(43), 434011 (2009).

1. Introduction

Hyperbolic metamaterials (HMMs) are subwavelength structures such as rod arrays [1–4] or multilayers [5,6] made to imitate “indefinite media,” a special case of extreme anisotropy where diagonal elements of the permittivity tensor have different signs (e.g., $\varepsilon_x = \varepsilon_z < 0$ and $\varepsilon_y > 0$) [7]. Such media are unusual because their dispersion relation $\omega^2/c^2 = (k_x^2 + k_z^2)/\varepsilon_z + k_y^2/\varepsilon_{xy}$ is hyperbolic rather than elliptical [Fig. 1(a)]. In the idealization that this relation holds for all $k_{x,y,z}$, different signs of $\varepsilon_{xy} = \varepsilon_z$ result in propagating solutions for waves with infinitely large wave vectors, i.e., $k^2 \gg \varepsilon_{xy}a^2/c^2$. Such waves (the “high-$k$ modes” [5–9]) are evanescent in isotropic media but become propagating in indefinite media. As a result, the photonic density of states (DOS) becomes unbounded, giving rise to new physical phenomena such as broadband spontaneous emission enhancement [5,6,10], anomalously high heat-transfer capabilities [11], and optical simulation of metric signature transitions [12]. Practical applications, e.g., near-field [13–15] and far-field subwavelength imaging (hyperlensing) [8,16] and highly absorptive “darker than black” coatings that benefit from surface roughness [17], were also proposed.

However, attributing the physics of HMMs to high-$k$ modes raises a few concerns. First, even though structural elements of an HMM, e.g., layer thicknesses in Fig. 1(b), may be much smaller than the vacuum wavelength at the frequency of interest, the wavelength of high-$k$ modes, $2\pi/k$, will eventually become even smaller. Therefore any real structure will have a
range of \( k \) where it is no longer “subwavelength” and can no longer be described by the effective medium approach [2,5,6], displaying pronounced optical nonlocality effects [20,21]. Hence, all conclusions about unbounded DOS in real HMMs become unreliable, and significant deviations from effective-medium predictions are expected in real HMMs [21–24], even when optical nonlocalities are taken into account in the homogenization theory [25].

Furthermore, the effective index approach does not explain the transition from a conventional material on a smaller (microscopic) scale to an HMM on a larger scale, and fails to provide any insight into the physical nature of high-\( k \) modes other than to assert that they must be bulk propagating waves. Such insight would be crucial to explore the extent to which these modes can be used as information carriers. Since the structures involved are metal-dielectric, it is strongly believed that high-\( k \) modes are plasmonic in nature. So various groups call them multilayer plasmons [26], Bloch plasmon polaritons [27], or volume plasmon polaritons (VPPs) [28], while other groups relate them to leaky waves in anisotropic waveguides [13, 29, 30] or to surface polaritons [4, 31]. In metal-dielectric multilayers, it is stipulated that these VPPs arise from surface plasmon polaritons (SPPs) at layer interfaces [14, 32]. However, the direct connection between an SPP at a single interface and a VPP in the multilayer HMM is still to be drawn, and the prevailing coupling mechanism between the SPPs is still not quite clarified [33].

In this paper, we provide a direct proof that a band of bulk propagating waves (VPPs) with large wave vectors in periodic multilayer HMMs originates from coupling of SPPs in the individual metal layers by virtue of the Bloch theorem. When the reflection coefficient of metal layers is replaced by a simple pole expansion that only preserves short-range SPP (SRSPP) excitations, correct dispersion relation of an HMM is recovered throughout its entire 1D Brillouin zone. We conclude that “high-\( k \) waves” in HMMs can be physically understood as “Bloch VPPs”, and can be seen as a distinct type of plasmonic excitations.

The paper is organized as follows. In Section 2, we review the basics of wave propagation in metal-dielectric multilayers, and discuss the dispersion relation for bulk waves in multilayer HMMs. In Section 3, we employ the pole expansion formalism to preserve only the SRSPPs in the metal layers, and show that bulk VPPs originate from surface-bound SRSPPs in the metal layers via the Bloch theorem. Finally, in Section 4 we summarize.
vector in metal or dielectric. (To fix the definition, we take $\text{Im} w_j \rho \equiv 0$.) The reflection and transmission coefficients of a metal layer are given by the Airy formulas,

$$ R_m = r_{dm} + t_{dm} t_{md} e^{2 \text{Im} w_j \rho d} \sin [1 - (r_{md} e^{2 \text{Im} w_j \rho d})^{-1}], \quad T_m = t_{dm} t_{md} e^{2 \text{Im} w_j \rho d} \sin [1 - (r_{md} e^{2 \text{Im} w_j \rho d})^{-1}]. \quad (2) $$

In Eqs. (1)–(2), $w_j = \sqrt{\varepsilon \omega^2 / c^2 - \kappa^2}$ (for $j = m,d$) is the $z$-directed component of the wave vector in metal or dielectric. (To fix the definition, we take $\text{Im} w_j \geq 0$; if $\text{Im} w_j = 0$ we take $\text{Re} w_j \geq 0$.) The reflection and transmission coefficients $r_{ij}$ and $t_{ij}$ at the $(i/j)$ interface are given by standard Fresnel formulas for $p$-polarized light,

$$ r_{md} = \frac{\varepsilon_m E_d - \varepsilon_d E_m}{\varepsilon_m E_d + \varepsilon_d E_m}, \quad r_{dm} = \frac{\varepsilon_d E_m - \varepsilon_m E_d}{\varepsilon_d E_m + \varepsilon_m E_d}, \quad t_{md} = \frac{2 \varepsilon_m \sqrt{\varepsilon_m \varepsilon_d}}{\varepsilon_m E_d + \varepsilon_d E_m}, \quad t_{dm} = \frac{2 \varepsilon_d \sqrt{\varepsilon_d \varepsilon_m}}{\varepsilon_d E_m + \varepsilon_m E_d}. \quad (3) $$

Assuming for now that the metal is lossless, we can conveniently label the plane wave components by a real tangential component $\kappa$ lying in the $x-y$ plane, as it does not vary across layers. Since the multilayer is periodic in $z$, it supports propagating Bloch waves with the wave vector $k^2 = k_B^2 + \kappa^2$. The relation between $k_B$ and $\kappa$ is given by the Bloch theorem [25, 32, 33]:

$$ \frac{\text{Tr} M_k}{2} = \cos [k_B (d_m + d_d)] = \cos (\varepsilon_m d_m) \cos (\varepsilon_d d_d) - (\eta + \eta^{-1}) \sin (\varepsilon_m d_m) \sin (\varepsilon_d d_d), \quad (4) $$

where $\eta = (\varepsilon_m \varepsilon_d) / (\varepsilon_d \varepsilon_m)$. As shown earlier (see, e.g., [26]), expanding Eq. (4) up to $(\varepsilon_m \varepsilon_d)^2$ reduces it to the hyperbolic dispersion equation, $\omega^2 / c^2 = k_B^2 / \varepsilon_m + \kappa^2 / \varepsilon_d$ where $\varepsilon_{m,d} = \rho \varepsilon_m + (1 - \rho) \varepsilon_d < 0$ and $\varepsilon_{m,d}^{-1} = \rho \varepsilon_m^{-1} + (1 - \rho) \varepsilon_d^{-1} > 0$ are the effective permittivity tensor components, and $\rho \equiv d_m / (d_m + d_d)$ is the metal filling fraction.

Figure 1(c) compares this approximate dispersion relation with the exact result of Eq. (4). As expected [25, 26], we see that VPPs in multilayer HMMs are indeed Bloch waves in a periodic metal-dielectric multilayer, approaching a hyperbolic dispersion relation for smaller $\kappa$ but deviating from it as $\kappa$ increases. The cut-off in the range of possible $\kappa$, $\kappa_{\text{max}} \approx 1 / (d_m + d_d)$ [24], puts a limit on the photonic DOS in real multilayers [see Fig. 1(d)]. For $\kappa \lesssim \kappa_{\text{max}}$, where the VPPs reach wavelengths as small as the layer thicknesses, the multilayer behaves like a photonic crystal rather than like a homogeneous effective medium, displaying a band structure. The hyperbolic dispersion relation comes from the local curvature of the propagation band near the $\Gamma$-point of the 1D Brillouin zone. In the HMM regime, the high-$k$ waves are backward-propagating [15, 21, 30].

The condition where the effective-medium approximation is valid, $w_j d_j \ll 1$, can be regarded as a special case of a “subwavelength condition” for HMMs, implying that neither the phase nor the amplitude of a propagating wave should vary significantly across the thickness of any layer in the structure. Unlike conventional media where the subwavelength condition can simply be $d_j / \lambda \ll 1$ due to the elliptical dispersion relation restricting the range of possible $\kappa$, the “HMM subwavelength condition” breaks down for some large $\kappa$ no matter how thin the layers are.

### 3. Pole expansion for surface plasmon polaritons in metal layers

Bloch waves in crystals are typically formed from elementary excitations in single elements (“atoms”) that couple in periodic systems to form bands. We can thus understand the underlying physics of HMMs by identifying the nature of the elementary excitations behind VPPs.
Although it has been generally understood that such excitations in metal-dielectric multilayers must be plasmonic in nature [21,26,27], a direct connection between SPPs at individual metal-dielectric interfaces and VPPs in HMMs can be established. To do so, we replace physical metal layers in an HMM by “fictitious” layers that only support one plasmonic mode, and compare the wave propagation properties in this fictitious structure with those in the original HMM.

From Eq. (1) we see that the Fresnel coefficients $R_m$ and $T_m$ play a central role in the dispersion relation, so the excitations we seek to characterize must be identified in these coefficients. Poles in the Fresnel coefficients signal the presence of guided wave-type excitations in multilayers. For example, SPPs at a single metal-dielectric interface are seen as poles in $r_{dm}$ and $t_{dm}$ [see Eq. (3)], but their wave number $\kappa_{dm}$, as given by the expression $\omega_m(\kappa_{dm})\epsilon_d + \omega_d(\kappa_{dm})\epsilon_m = 0$, is on the order of $(\omega/c)\sqrt{\epsilon_d}$ at optical frequencies. What we must clarify is how the wave vectors of VPPs in HMMs become enormously large ($\kappa \gg \kappa_{dm}$).

In thin metal layers, comprising two metal-dielectric interfaces, SPPs are known to couple either symmetrically or antisymmetrically, producing long-range SPPs (LRSPPs) or short-range SPPs (SRSPPs), respectively. Both are described by the pole condition in Eqs. (2),

$$1 - r_{dm}^2 e^{2i\omega_m d_m} = 0$$

(5)

Asymmetric coupling in SRSPPs makes their wave vectors larger than for LRSPPs. Assuming that $\omega^2 > \epsilon_m d_m \omega_0^2/c^2$, we solve Eq. (5) to obtain a limit for the SRSP wave number for $d_m \rightarrow 0$: $\kappa_{sp} \approx (\ln r)/d_m, r = (\epsilon_m - \epsilon_d)/(\epsilon_m + \epsilon_d)$. We see that $\kappa_{sp}$ becomes very large as $d_m$ decreases, confirming that the involvement of SRSP in the VPP formation is a well-justified conjecture.

To confirm the validity of this conjecture and to see that SRSPPs are crucial in the dispersion relation of HMMs, we replace the expressions for $T_m$ and $R_m$ in Eq. (1) by their pole expansion around the SRSP pole at $\kappa_{sp}$: $T_m = \tau_m/(\kappa - \kappa_{sp}), \tau_m \approx (r^{-1} - r)/(2d_m)$. Note that as $\kappa \rightarrow 0, T_m \rightarrow -\tau_m/\kappa_{sp} \approx 1$, in agreement with the complete transmission of a very thin ($d_m \ll c/\sqrt{\epsilon_m/\omega}$) metal film. The corresponding pole expansion for $R_m$ would give $-\tau_m/\kappa - \kappa_{sp}$. However, to stay consistent with vanishing reflectivity for a very thin metal film at normal incidence we add a constant to this expression

$$R_m = -\tau_m/(\kappa - \kappa_{sp}) - (\tau_m/\kappa_{sp}), \quad T_m^2 - R_m^2 = -2\tau_m^2/[\kappa_{sp}(\kappa - \kappa_{sp})] - (\tau_m/\kappa_{sp})^2.$$  

(6)

Substituting Eq. (6) in Eq. (1), instead of Eq. (4) we get

$$\cos [KB(d_m + d_d)] \approx [1 - (\kappa - \kappa_{sp})/(2\tau_m)] e^{i\omega_m d_d} + [(\kappa - \kappa_{sp})/(2\tau_m)] e^{-i\omega_m d_d}.$$  

(7)

In Fig. 2(a), it can be seen that Eq. (7) provides a good approximation for Eq. (4). The agreement remains reasonable for $\rho$ up to 0.5, getting slightly better for smaller $\rho$, and persists for lossy metals. Interestingly, omitting the second terms in Eqs. (6) [using just $R_m = -\tau_m/(\kappa - \kappa_{sp})$] can also achieve a decent agreement between Eqs. (7) and (4) in the range of larger $c\kappa/\omega$ with $\kappa$ near $\kappa_{sp}$, which is the region of most VPPs [Fig. 2(b)]. However, adding the correction term drastically improves the agreement near $k_B = 0$ where $c\kappa/\omega$ is smaller, making the pole approximation accurate throughout the entire Brillouin zone.

It is also remarkable that the pole expansion (6) continues to give a correct dispersion relation for smaller $\rho < \epsilon_d/(\epsilon_m + \epsilon_d)$, where $0 < \epsilon_{xy} < \epsilon_x$, and the structure is no longer an HMM but an extremely anisotropic medium. As seen in Fig. 2(c), the exact dispersion relation has two branches [21]. Only the inner, low-$k$, forward-wave branch is recovered by the effective medium approximation, which may lead to an erroneous conclusion that high-$k$ waves disappear for smaller filling fractions. In fact, high-$k$ waves are still contained in the other (outer) branch, which gets pushed to higher $\kappa$, outside of the validity of the condition $\omega_m d_m \ll 1$. This backward-wave branch is correctly recovered by the pole expansion, indicating (in line
with the results of [21]) that VPPs in metal-dielectric multilayers also exist when the HMM requirements are not met.

For higher metal filling fractions, $\rho > 0.5$, it would be expected that the dispersion relation should be more accurately recovered by the pole expansion for a thin metal-dielectric-metal gap waveguide rather than a metal layer [33]. The corresponding expressions can be obtained from Eqs. (6)–(7) with the subscripts $m$ and $d$ interchanged. However, the agreement with the exact Eq. (4) is only slightly better than Eq. (7) for $0.5 < \rho < -\varepsilon_m/(\varepsilon_m + \varepsilon_d) \approx 0.8$, so Eq. (7) remains a good approximation throughout the HMM parameter range.

Finally, note that there is surely more to the Fresnel coefficients $R_m$ and $T_m$ than SRSPPs. For example, LRSPPs are signaled by the presence of poles in those coefficients as well. However, the width of the LRSPP poles is much narrower in $\kappa$, and they do not have any influence on the dispersion relations at large $c\kappa/\omega$.

4. Conclusions

We have investigated electromagnetic wave propagation in multilayered metal-dielectric hyperbolic metamaterials (HMMs). Starting with the assumption that the only excitation supported by a thin metal film is an SRSPP, and coupling these excitations together through dielectric layers, we have reproduced the correct dispersion relation of “high-$k$ waves” in a multilayer HMM throughout its 1D Brillouin zone. Hence, propagating waves in metal-dielectric multilayers, including HMMs, can indeed be understood as bulk plasmonic waves or VPPs arising from the coupling between SRSPPs in the constituent metal layers. In analogy with 2D arrays of plasmonic nanoparticles, where localized particle plasmons couple to form surface waves called Bloch SPPs [35], we can understand high-$k$ propagating waves in HMMs as Bloch VPPs.

Acknowledgments

The authors thank V. Babicheva, E. Narimanov and M. Liscidini for helpful suggestions. This work was supported by the Natural Sciences and Engineering Research Council of Canada. One of us (S.V.Z.) wishes to acknowledge financial support from the People Programme (Marie Curie Actions) of the European Union’s 7th Framework Programme FP7-PEOPLE-2011-IIF under REA grant agreement No. 302009 (Project HyPHONE).