ABSTRACT
The Goal is to obtain a simple multichannel source separation with very low latency. Applications can be teleconferencing, hearing aids, augmented reality, or selective active noise cancellation. These real time applications need a very low latency, usually less than about 6 ms, and low complexity, because they usually run on small portable devices. For that we don’t need the best separation, but “useful” separation, and not just on speech, but also music and noise. Usual frequency domain approaches have higher latency and complexity. Hence we introduce a novel probabilistic optimization method which we call ”Random Directions”, which can overcome local minima, applied to a simple time domain unmixing structure, and which is scalable for low complexity. Then it is compared to frequency domain approaches on separating speech and music sources, and using 3D microphone setups.

Index Terms— Zeroth-Order Optimization, Random Directions, multichannel source separation, low delay separation

1. INTRODUCTION
The goals of this paper are to obtain a simple multichannel source separation with very low latency. Applications for it can be teleconferencing, hearing aids, augmented reality, or selective active noise cancellation. These real time applications need a very low latency, usually less than about 6 ms. Also those applications need separation not just for speech, but also for music and noise.

Previous approaches usually use the frequency domain for separation, usually using the Short Time Fourier Transform (STFT). Their STFT typically has a block size of 4096, and hop size of 2048 samples. The hop size alone leads to an algorithmic delay of 2047 samples. This is 128ms at 16 kHz sampling rate, which is too much for our applications. Examples for the frequency domain separation are FastMNMF [1] or AuxIVA [2].

To obtain the least possible algorithmic delay, the time domain should be used for separation instead, which means to use time-domain unmixing filters, like ”Trinicon” [3], which uses FIR unmixing filters. This leads to objective functions for finding the systems parameters which can be highly non-convex, for which the usual gradient based methods usually fail. Hence the presented approach uses a zeroth-order optimization method instead, the method of Random Directions, which is more robust against local minima. A difference in practice is that probabilistic methods don’t have exactly the same results every time they are executed, hence the computation of the standard deviations of the results is also important.

2. NEW APPROACH
The presented new approach uses the time domain, with a fractional delay IIR filters [4] and attenuation factors. This models the propagation delays of the sources between the microphones, together with an attenuation factor. These fractional delays and attenuation factors are the unmixing coefficients which the optimization has to find.

2.1. Parallel Processing
The determination of suitable unmixing filters takes some signal time. To avoid this causing a delay, it can be computed in a parallel thread, while already processing the signal in the time domain. This means the separation in the beginning is not at its best, but it improves quickly as more of the signal is processed. In this way an algorithmic delay in the order of the fractional delays between the microphones is possible.

These are the two parallel threads,

• unmixing in the time domain,

• periodic optimization of the unmixing coefficients in a parallel thread.

2.2. Signal Accumulation
The processing complexity for the unmixing coefficients increases with the signal length. To reduce this complexity, the signal can be ”accumulated” in a short signal block of about
0.5s length. The assumption for it is that the solution for the coefficients is not changed by this pre-processing. It can even argued that this suppression of the signal with itself may help the optimization, since it makes the signal more broadband. This is shown in the following code:

```python
blocksize=8000; blockno=0
for i in range(min(blocks,16)):
    # accumulate audio blocks over ca. 3 sec:
    blockaccumulator=0.98*blockaccumulator + 0.02*X[blockno*blocksize+np.arange(blocksize)]
    blockno+=1
```

### 2.3. The Unmixing Function

Let $S$ be the number of sources, $M$ be the number of microphones, $X_i(z)$ be the $i$-th microphone signal in the $z$-domain, $Y_i(z)$: the $i$-th separated source, with $a$ being the attenuation factors and $d$ the fractional delays, and with the signal vectors,

$$ X = [X_1(z), \ldots, X_M(z)], \quad Y = [Y_1(z), \ldots, Y_S(z)] $$

Then the unmixing function of the presented method is,

$$ X \cdot \begin{bmatrix} a_{1,1}z^{-d_{1,1}} & \ldots & a_{1,S}z^{-d_{1,S}} \\ \vdots & & \vdots \\ a_{M,1}z^{-d_{M,1}} & \ldots & a_{M,S}z^{-d_{M,S}} \end{bmatrix} = Y $$ (1)

This models the delays and attenuations from a source signal between the different microphones. Observe that it does not model the room impulse response, hence the effect of the room on the sound is not canceled.

### 2.4. The Objective Function

The objective function for the optimization should be a measure of statistical independence between the separated sources. Mutual information would measure it, but it is complex to compute. instead, the negative Kullback-Leibler divergence between all pairs of separated sources is used. The shown example has only one source pair, for simplicity. Since a possible minimum of the objective function is also obtained by setting an output source simply to zero, or very small values, we also include a power preservation coefficient $P = |1 - power_{in}/power_{out}|$. The Kullback-Leibler Divergence $D_{KL}$ indicates how different 2 signals are, hence we want to minimize its negative value for the output sources. A Lagrange multiplier is used to combine those two functions into one objective function $f = -D_{KL} + \lambda \cdot P$. The Lagrange multiplier $\lambda$ was set to 0.1.

The objective function “together with the unmixing function represents a very non-convex objective function with many local minima. Hence the zeroth-order optimization of [5] is used, which turns out to be relatively robust against local minima, and which is described next.

### 3. ZEROTH-ORDER OPTIMIZATION

Zeroth-order optimization uses no gradient, unlike the commonly used Gradient Descent algorithm, or its use in the LMS algorithm. Gradient Descend can be seen as first-order optimization, with its use of the gradient, and is robust and fast for convex objective functions, but for non-convex objective functions it will become stuck at the nearest local minimum. That is why, for the presented system, Gradient Descent does not work, and an alternative is needed. Here, the Gradient is not really helpful, and it could as well be replaced by a random vector over a given search space. This then leads to zeroth-order optimization. Zeroth-order optimization can basically be used where Gradient Descent was used, like for online optimization. An overview can be found in [6]. Examples are also Random Pursuit [7], and Gradientless Descent [8].

#### 3.1. The Method of Random Directions

The proposed method of Random Directions has the advantages that it is relatively fast and has a robust convergence for our applications; It is not increasing the objective function, hence its application does not make things worse for difficult objective functions; and it is still fast for higher coefficient dimensions.

In the following pseudo code, Algorithm 1, shows the method of Random Directions. In the beginning it is initialized with a random starting vector $x_0$, the desired number of iterations $T$, and parallel processes $P$. Then there is a “scale” parameter. This defines the size of the search area, the standard deviation of the random search vector. In the beginning of the iterations this has a larger value, starting with "startingscale". In the presented experiment it was 4.0. The scale of the search vector is reduced over the duration of the iterations in a non-linear way, until it reaches "endscale", which was chosen as 0.0 in the presented experiment. Next there is a parallel search using $P$ randomly generated search vectors $v_p$. This is done on a random subspace of coefficients, to make it more robust for higher dimensions. Non-adaptive random subspaces are used, here of dimension 8. This means only 8 entries of $v_p$ are non-zero.

From these search vectors, the index of the best vector is obtained, and then tested if it found a new minimum of the objective function $f$. If so, the algorithm uses a coarse line search for the successful search vector. It was found that this speeds up convergence in more smooth areas of the objective function. See also [5]. A simpler version for 2-channel source separation was described in [9] [10].

Note that the algorithm only makes an update if the objective function became smaller. This ensures that the application of this method can only improve, but not degrade the performance, an important property for hard to optimize objective functions. The number of iterations $T$ is chosen ac-
Input: $f(x): \mathbb{R}^n \to \mathbb{R}$: Objective function to be minimized
$x_0$: Starting point vector,
T: Number of iterations,
Number of parallel processes,
startingscale: Standard deviation at the start
endscale: Standard deviation at the end
Initialization: $x_{\text{best}} = x_0$
for $m=0,...,T$ do
  scale = endscale + (startingscale - endscale) · ((1.0 - m/iterations)$^2$
  Parallel Processing:
  generate search vectors $v_p$ with std deviation "scale" and zero mean on random subsets of coefficients;
  compute $f(x_{\text{best}} + v_p)$
  $p_{\text{best}} = \arg \min_p \{f(x_{\text{best}} + v) \mid v = v_p\}$
  if $f(x_{\text{best}} + v_{p_{\text{best}}}) < f(x_{\text{best}})$ then
    Find new $x_{\text{best}}$ with coarse line search along successful vector $v_{p_{\text{best}}}$,
    $k_{\text{best}} = \arg \min_k f(x_{\text{best}} + 2^k v_{p_{\text{best}}})$,
    $k = (-8, \ldots, 8)$ (Line search)
    $x_{\text{best}} = x_{\text{best}} + 2^{k_{\text{best}}} v_{p_{\text{best}}}$
  end
end
return $x_{\text{best}}$

Algorithm 1: The method of Random Directions.

cording to the power of the available processors. The higher
the better, but it still needs to be able to run in real-time. In the
presented experiment $T = 1000$ was used. For the number of
parallel processes usually the available number of processors
(CPU’s) can be chosen. In the presented experiments it was $P = 8$.

3.1.1. Probabilistic Background

To see how this algorithm works from the probabilistic view-
point, let’s assume $x_0$ is the current starting vector or starting
point, and $v_p$ a random search vector, drawn from a symme-
trical independent Gaussian probability distribution (the covari-
ance is a diagonal matrix) with zero mean, a given standard
deviation $\sigma$ (the "scale"), and with $N$ the dimension of the
search subspace,

$$p(v_p) = \frac{1}{\sigma^N \sqrt{(2\pi)^N}} \cdot e^{-\frac{1}{2}(|v_p|^2)}.$$  \hspace{1cm} (2)

Let’s further assume $v_\ast$ is the vector to the true absolute min-
imum, hence at position $x_0 + v_\ast$. Let $V$ be a region around
$v_\ast$ such that the objective function in that region is smaller
than its current value (assuming it is not already in a global
minimum). Hence if $v_p \in V$, then $f(x_0 + v_p) < f(x_0)$. To es-
timate the probability of success with a search vector, it is as-
sumed that $p(v_p)$ is approximately constant over our relatively
small region $x_0 + V$, and the volume of our N-dimensional
region $V$ is $\text{Vol}(V)$. Then the probability of success, hitting
this region, is approximately

$$p(v_p \in V) \approx p(v_\ast) \cdot \text{Vol}(V).$$  \hspace{1cm} (3)

To maximize the probability of success with the random search
vectors, $p(v_\ast)$, Eq. (2) needs to be maximized, with
a properly chosen standard deviation $\sigma$. This maximum is
obtained with

$$\sigma = |v_\ast|/\sqrt{N},$$  \hspace{1cm} (4)

This means a proper guess of the distance to the minimum
gives a good estimate for the "scale" $\sigma$. Since it can be as-
bsumed that the distance to the minimum is iteratively reduced,
the "scale" needs to be reduced accordingly. This is what
the algorithm is doing with the shrinking of the scale from
"startingscale" to "endscale". Eq. (2) also shows that for $\sigma > 1/\sqrt{(2\pi)}$ the probability of success, eq.(3), is reduc-
ing exponentially with the subspace dimension $N$. Hence at
least in the beginning, for larger distances from the minimum,
it is useful to reduce the dimension using subspaces.

4. COMPARISON, EVALUATION

As comparison method “Trinicon” is chosen, because it is also
a time domain method. The used implementation is of the
"pyroomacoustics" Python module. For a more precise
comparison, the same parallel processing was applied. For
both, the first ca. 8 seconds of the signal were used to ob-
tain the optimized filter coefficients. These filter coefficients
where then used to unmix the entire signal, for simplicity.

The used audio sources are pairs from speech, and also
noise, and music: Synthetic male speech from "espeak" [11]
("espeak_wav_{16}.wav"), synthetic female speech ("espeak-
female_{16}.wav"), pink noise from "csound" [12] ("pink-
ish16.wav"), tones from "csound" ("oscili_test_{16}.wav"),
and music from [13] ("fantasy-orchestra_m16.wav"). The
pairs where ("espeakfemale_{16}.wav", "espeak_wav_{16}.wav"),
("pinkish16.wav", "espeakwav_{16}.wav"), ("oscili_test_{16}.wav", 
"espeakwav_{16}.wav"), ("fantasy-orchestra_m16.wav", "es-
peakwav_{16}.wav"). They have a sampling rate of 16 kHz and
lengths between 6.3s and 11.8s. The average length of the
pairs (where the shorter signal of a pair is zero padded to the
length of the longer signal) is 8.4s. The shown processing
times in Table (1) are from a computer with an Intel(R)
Xeon(R) W-2123 CPU @ 3.60GHz, with 8 CPU’s. As long
as the processing time is below the signal length, the system
is real-time capable. Table (1) shows that for the stereo case,
Random Directions online has a mean processing time of
2.83s, with standard deviation of 0.16s. This is about 3 times
faster. The longest processing time is observed for the case
of the cube microphone setup, with mean 4.57s and standard
deviation of 0.18s. This means that the clock frequency could
be reduced until real time processing speed is reached. If a
further reduction on hardware requirements is desired, the number of iterations and of parallel processes can be reduced, at the cost of a gradual reduction of separation performance. Also observe that Trinicon has a shorter processing time.

4.1. Microphone Setups and Simulated Room

3 microphone setups where tested: A stereo microphone pair, 20cm apart; a square of 4 microphones, 20cm side length; and a cube of 8 microphones, 20cm side length. The room was simulated with the Python module "pyroomacoustics" [14]. The room dimensions are 5m by 4m by 2.5m, and the reverberation time was chosen as \( r_t = 0.1 \) s. Two source where used for the evaluation, at coordinate positions [2.5m, 1.5m, 1.50m] and [2.5m, 3.3m, 1.50m]. The microphones where centered around coordinates [3.1m, 2.1m, 1.2m], Fig. (1).

![Simulated room with cube microphone setup. The dots are the two sources, the crosses are the microphones.](image)

4.2. Evaluation

As evaluation, the Python module "mir_eval" was used [15]. It computes the "Signal to Distortion Ratio" (SDR, linear distortions, like filtering), the "Signal to Interference Ratio" (SIR), and the "Signal to Artifacts Ratio" (SAR, the non-linear distortions). These measures are computed and then averaged over the different source pairs, and the standard deviation is computed. Since the presented Random Directions algorithm is probabilistic, each setup was repeated 10 times. These sets became part of the averaging and the computation of the standard deviations. Here the most interesting measures are the SIR, as a measure for the separation performance, and the SAR, because it measures the non-linear distortions, at which the presented algorithm should be particularly good at. The SDR measure is less interesting here, because it measures linear distortions, like a filtering effect from the room, which the presented method is not removing and was not a goal.

### Table 1. Evaluation of the source separation for different methods and setups. "Mean" is the mean over all sources, and "std.dev." their standard deviation.

| method          | SIR  | SAR   | Time | Setup |
|-----------------|------|-------|------|-------|
| randdironline   | mean | 9.37  | 33.02| stereo|
| randdironline   | std. dev. | 4.71  | 8.47 | 0.16  | stereo|
| randdironline   | mean | 8.03  | 31.28| square|
| randdironline   | std. dev. | 5.48  | 6.6  | 0.15  | square|
| randdironline   | mean | 4.22  | 30.21| cube  |
| randdironline   | std. dev. | 3.44  | 5.83 | 0.18  | cube  |
| trinicononline  | mean | 3.38  | 18.84| stereo|
| trinicononline  | std. dev. | 1.02  | 4.58 | 0.02  | stereo|
| trinicononline  | mean | 0.98  | 18.06| square|
| trinicononline  | std. dev. | 0.36  | 1.43 | 0.01  | square|
| trinicononline  | mean | 1.04  | 19.99| cube  |
| trinicononline  | std. dev. | 0.63  | 3.52 | 0.03  | cube  |
| fastmnmf        | mean | 20.16 | 14.51| stereo|
| fastmnmf        | std. dev. | 7.99  | 5.34 | 1.49  | square|
| fastmnmf        | mean | 12.72 | 7.92 | 23.55 | cube  |
| fastmnmf        | std. dev. | 8.87  | 3.79 | 5.84  | cube  |
| auxIVA          | mean | 14.72 | 14.14| stereo|
| auxIVA          | std. dev. | 12.3  | 6.1  | 0.22  | stereo|
| auxIVA          | mean | 19.7  | 5.54 | 0.49  | square|
| auxIVA          | std. dev. | 12.38 | 2.97 | 0.11  | square|
| auxIVA          | mean | 16.67 | 2.66 | 1.28  | cube  |
| auxIVA          | std. dev. | 11.28 | 1.77 | 0.27  | cube  |

4.3. Results

Between the 2 online algorithms, the best SIR (separation) is achieved by the presented Random Directions method, with 9 dB for the stereo case. The 9 dB sound like a clear separation, with some slight audible crosstalk from the other source. 3 dB SIR, on the other hand, sounds like no audible separation. The best overall SAR (non-lin. distortions) is achieved also with the Random Directions, with 33 dB for the stereo case. There was indeed no audible non-linear distortion. The best overall SIR, including offline methods, is achieved by FastMNMF with 20 dB for the stereo case. In this case there is no audible crosstalk from the other source. This difference can also be seen as the price for low delay separation, although both sound sufficiently separated. Due to its stochastic nature, Random Directions also has the highest standard deviations, which means sometimes it works better than at other times. This can be also be seen in Fig. 2 a box plot with the middle 2 quartiles for a single source pair for 10 runs of Random Directions. It still works for more microphones (square,
Fig. 2. Box plots of SDR, SIR, SAR and processing time for Random Directions for the square microphone case, for an individual item pair (‘espekfemale’, ‘espeakwav’). The boxes represent the middle two quartiles.

cubic), but declines somewhat in separation performance, but not as much as Trinicon. A full software demo with listening examples in a Jupyter Colab notebook can be found at [16].

5. CONCLUSIONS

The method of Random Directions can successfully optimize the very non-convex objective function for audio separation in the time domain for low delay online applications. It also works for non-speech signals and more microphones. Using this zeroth-order optimization method made finding of a globally good solution possible, since the objective function is highly non-convex, which makes gradient based optimization methods fail. The method of Random Directions is strictly decreasing the objective function, has a line search along successful directions for increasing speed for “well behaved” objective functions, and uses a random subspace approach to make it more robust to higher dimensions, meaning more coefficients to optimize. The results showed that it compares favourably to Trinicon in SIR and SAR, and to frequency domain methods in terms of the SAR measure.

6. REFERENCES

[1] K. Sekiguchi, A. A. Nugraha, Y. Bando, and K. Yoshii, “Fast multichannel source separation based on jointly diagonalizable spatial covariance matrices,” in EU-SIPCO, 2019.

[2] N. Ono, “Stable and fast update rules for independent vector analysis based on auxiliary function technique,” in Proc. IEEE, WASPAA, 2011.

[3] R. Aichner, H. Buchner, F. Yan, and W. Kellermann, “A real-time blind source separation scheme and its application to reverberant and noisy acoustic environments,” Elsevier Signal Processing, 2006.

[4] I. Senesnick, “Low-pass filters realizable as all-pass sums: design via a new flat delay filter,” IEEE Transactions on Circuits and Systems II, 1999.

[5] G. Schuller and O. Golokolenko, “Probabilistic optimization for source separation,” in Asilomar Conference on Signals, Systems, and Computers, Asilomar, CA, USA, Nov 2020.

[6] S. Liu, P. Y. Chen, B. Kailkhura, G. Zhang, A. O. Hero III, and P. K. Varshney, “A primer on zeroth-order optimization in signal processing and machine learning: Principals, recent advances, and applications,” IEEE Signal Processing Magazine, vol. 37, no. 5, pp. 43–54, 2020.

[7] Sebastian U. Stich, Christian L. Müller, and Bernd Gärtner, “Optimization of convex functions with random pursuit,” arXiv, vol. 1111.0194, 5 2012.

[8] Daniel Golovin, John Karro, Greg Kochanski, Chansoo Lee, Xingyou Song, and Qiuyi Zhang, “Gradientless descent: High-dimensional zeroth-order optimization,” arXiv, vol. 1911.06317, 5 2020.

[9] Oleg Golokolenko and Gerald Schuller, “Fast time domain stereo audio source separation using fractional delay filters,” in 147th AES Convention, New York, NY, USA, October 16-19 2019.

[10] Oleg Golokolenko and Gerald Schuller, “A fast stereo audio source separation for moving sources,” in Asilomar Conference on Signals, Systems, and Computers, Asilomar, CA, USA, Nov 3-6 2019.

[11] Espeak, http://espeak.sourceforge.net/.

[12] Csound, https://github.com/csound/csound.

[13] Freesound, https://freesound.org.

[14] Robin Scheibler, Eric Bezzam, and Ivan Dokmanić, “Pyroomacoustics: A python package for audio room simulations and array processing algorithms,” arXiv, vol. 1710.04196, 2017.

[15] C. Raffel, B. McFee, E. J. Humphrey, J. Salamon, O. Nieto, D. Liang, and D. P. W. Ellis, “mir_eval: A transparent implementation of common mir metrics,” in Proceedings of the 15th International Conference on Music Information Retrieval, 2014.

[16] Low Delay Multichannel Source Separation Random-Directions Demo, https://github.com/TUIlmenauAMS/LowDelayMultichannelSourceSeparation_Random-Directions_Demo.