RE$_2$O$_3$ Nanoparticles Embedded in SiO$_2$ Glass Matrix — A Colossal Dielectric and Magnetodielectric Response

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Abstract

Significant experimental effort has been inspected to consider and implement favorable high-$k$ gate dielectrics with magnetodielectric (MD) effect of series of rare earth oxide (RE$_2$O$_3$, RE ~ rare earth ions) nanoparticles (NPs) embedded in sol–gel derived SiO$_2$ glass matrix. Properly calcined RE$_2$O$_3$ NP-glass composite systems (in which RE ~ Sm, Gd and Er) show an intriguing colossal enhancement of dielectric constant along with MD effect near room temperature. The enhancement of dielectric constant is closely related to oxygen vacancy induced dielectric relaxation (or, more correctly, particle size effect from different calcined temperature), reconstructed from extended X-ray absorption fine structure. The MD response is strongly depended on the superparamagnetic property of the rare earth ions. From application point of view, the enhancement of dielectric constant associated with MD response can be achieved by tuning the NPs size through varying annealing temperature and/or increasing the doping concentration of magnetic rare earth oxide, which will be the key guidelines to accomplish the compatibility, performance and reliability requirements for future complementary metal-oxide-semiconductor (CMOS) technology.

Keywords: Rare earth oxide nanoparticle, high-$k$ materials, magnetodielectric effect, diffuse phase transition

1. Introduction

Tiny electrical components are now unanimously required to be high in functionality and reliability and low priced in response to progress in the high density mounting technology.
Continued device scaling for future technology nodes requires reduction in equivalent oxide thickness (EOT) of gate dielectrics to maintain electrostatic control of the charges induced in the channel. The use of amorphous SiO$_2$ as a gate dielectric offers several key advantages in complementary metal-oxide semiconductor (CMOS) processing, including thermal and chemical stability as well as superior electrical isolation properties (high band gap of nearly 9 eV, and a Si–SiO$_2$ potential barrier for electrons of about 3 eV). The continuous miniaturization of Si electronics has imposed severe constraints on the performance of the SiO$_2$ gate oxide, with its thickness now approaching the quantum tunneling limit [1,2]. To continue the downward scaling, dielectrics with a higher dielectric constant (high-$k$) are being suggested as a solution to achieve the same transistor performance while maintaining a relatively thick physical thickness. Following this roadway, many materials systems (viz. lead–free non-ferroelectric) are currently under consideration as alternatives to conventional silicon oxide films as the gate dielectric material for sub-0.1 μm CMOS technology. Such an approach allows one to employ the best available materials for each phase, whose properties are known a priority due to the scarcity of high-$k$ materials, to suit the desired application. Recent reports of giant dielectric constant have directed considerable attention to several new material systems, such as perovskite–related materials ACu$_3$Ti$_4$O$_{12}$ ($A = \text{Ca, Bi}_{2/3}\text{Y}_{2/3}\text{La}_{2/3}$) [3,4], La$_{2/3}$Li$_x$Ti$_{1-x}$Al$_x$O$_3$ [5], Nd$_2$O$_3$ doped (1-$x$)Bi$_{0.5}$Na$_{0.5}$TiO$_3$ (0.005 ≤ $x$ ≤ 0.025) [6], Fe-containing complex perovskites A(Fe$_{1/2}$B$_{1/2}$)O$_3$ ($A = \text{Ba, Sr, Ca; B = Nb, Ta, Sb}$) [7,8], non-perovskite material Li$_{0.05}$Ti$_{0.02}$Ni$_{0.93}$O [9], percolative BaTiO$_3$–Ni composites [10], electron-doped manganites Ca$_{1-x}$La$_x$MnO$_3$ and hole-doped insulators La$_2$Cu$_{1-x}$Li$_x$O$_4$ and La$_{2.2}$Sr$_x$NiO$_4$ [11–13]. The sensitivity of these complex oxides to strain, stoichiometry, phase heterogeneities, oxidation state, disorder, etc. can lead to drastic modifications in their magnetic and electric properties at the nanoscale. Besides that, as the key guidelines for replacing alternative dielectrics with high-$k$ materials are required to (i) remain thermodynamically and chemically stable between the metal-oxide and Si substrate; (ii) kinetic stability against Si and the metal gate, in particular during high temperature processing and annealing; (iii) insulating properties: band offsets with Si over 1 eV to assure low leakage currents; (iv) a passivated, low-defect-density interface with Si to ensure large carrier mobility in the Si channel and good breakdown properties; and (v) interface quality between the high-$k$ dielectrics and Si substrate: a low defect density in the high-$k$ dielectric itself to prevent flat band and threshold voltage shifts and instabilities. Many dielectrics appear favorable in some of these areas, but very few materials are promising with respect to all of these guidelines. The ranking of HfO$_2$-based system as a desired high-$k$ gate dielectric material to replace amorphous SiO$_2$ drops considerably, as HfO$_2$ suffers crystallization at a relatively low process temperature (< 500°C), resulting high leakage current along the grain boundaries [14]. Therefore, the exploitation of new type of amorphous phase pure high-$k$ gate dielectrics candidates as a replacement of SiO$_2$ still faces several daunting challenges.

Besides the aforementioned consideration, the superior electrical characteristics of the Si–SiO$_2$ interface in ideal gate dielectric stack compatible with planarization technology has not achieved with any other alternative semiconductor–dielectric combination. Despite several key advantages of SiO$_2$, the continual scaling of CMOS technologies has pushed the Si–SiO$_2$ system in formidable challenge. One promising alternative approach to overcome the scaling limit has been proposed to substitute by silica-based single-valence nanoparticles (NPs) as gate
insulator (interface between silicon and NP-oxides embedded silica), where flexibility, compatibility and functionality may be achieved through different NPs sizes/concentrations. Concentrating on the desired NP-oxides, potentially stable rare earth oxides ($\text{RE}_2\text{O}_3$, $\text{RE} \sim \text{rare earth}$, a series of elements from La to Lu with stable $\text{RE}^{3+}$) were chosen, which are attractive materials based on good thermodynamic energy considerations with silicon, highly resistive and a high conduction band offset over 2 eV. We have presented extensive results, providing useful insight into the physics of nano-composite high-$k$ gate dielectrics. Sol–gel derived non-magnetic SiO$_2$ glass matrix with magnetic/nonmagnetic rare earth NP-oxides provides a convenient way to tailor desired magnetic, dielectric (in presence of applied magnetic field), and other properties by altering the type, size and concentration of the dopant ions.

2. Sample preparation

The preparation of $\text{RE}_2\text{O}_3$:SiO$_2$ nano-glass composite system ($\text{RE} \sim \text{La, Nd, Sm, Eu, Gd, Dy, Ho, Er, Tm, Yb and Lu}$) consists of three consecutive processes: (a) preparation of wet gel in which rare earth ions were doped by sol–gel way, (b) drying of the gel and (c) densification of the dry gel to a dense glass in which $\text{RE}_2\text{O}_3$ NPs embedded by calcining at selective temperatures [15]. The process was based on the hydrolysis of precursors, such as tetraethylorthosilicate [Si(OC$_2$H$_5$)$_4$] (TEOS) and subsequent condensation of hydrolyzed TEOS in a medium containing a hydroalcoholic solution of rare earth salt [16] (Figure 1(a)) having different mol% concentrations following essentially the method developed by Sakka and Kamiya [17]. Water was required for the hydrolysis. The molar ratio of water and TEOS was kept at 20 while that of TEOS and catalyst HCl at 100. Dry ethanol was used for diluting the alkoxide. The following composition of the Si(OC$_2$H$_5$)$_4$ solutions used in the study (Table 1):

| Si(OC$_2$H$_5$)$_4$ (gm) | H$_2$O (gm) | C$_2$H$_5$OH (gm) | Mole ratio of H$_2$O to Si(OC$_2$H$_5$)$_4$ | Volume (gm/100 cc) | SiO$_2$ content (gm) |
|-------------------------|-------------|------------------|-----------------------------------------|-------------------|-------------------|
| 169.5                   | 292.8       | 37.5             | 20                                      | 500               | 9.80              |

Table 1. Compositions of the Si(OC$_2$H$_5$)$_4$ (TEOS), H$_2$O, and C$_2$H$_5$OH solutions used in the sol–gel process.

There are two distinct chemical reactions involved in the sol–gel process, describing Eqn. (1) for hydrolysis of the alcohol groups, Eqns. (2) and (3) for polycondensation of hydroxyl groups.

a. Hydrolysis:

$$\equiv \text{Si-OR} + \text{H}_2\text{O} \rightarrow \equiv \text{Si-OH} + \text{ROH} \quad (1)$$

b. Condensation (water/alcohol condensation):

i. Water condensation:
Hydrolysis:
\[ \equiv \text{Si-OH} + \equiv \text{Si-OH} \rightarrow \equiv \text{Si-O} \equiv + H_2O \]  

(2)

Alcohol condensation:
\[ \equiv \text{Si-OH} + \equiv \text{Si-OR} \rightarrow \equiv \text{Si-O-Si} \equiv + \text{ROH} \]  

(3)

The clear solutions without any precipitation are prepared with the mixing of half amount of ethanol in alkoxide and the solution consisting of the specified amount of water with another half of the ethanol containing HCl and dopant. The mixture solutions continued stirring for 2–3 hours at room temperature. The clear solution was kept in pyrex beaker at the atmospheric condition for 7/8 days to form stiff monolithic transparent gel. Further, the gels were allowed to dry for 4–5 weeks at room temperature. The dried (liquid removed by thermal evaporation) monolith is termed as xerogel. The oven–dried gel (temperature range 100–200°C) still contains large concentration of chemisorbed hydroxyls. Heat treatment in the temperature range 500–800°C desorbs the hydroxyls, forming a stabilized gel. At 1000°C, it transformed to a dense glass. Heat treatments of samples were performed according to preselected calcination temperature schedule [16] (Figure 1(b)).

Figure 1. (Color online) (a) Sol–gel process. (b) Gel–glass embedded with rare earth nanoparticle calcination process.

It is relevant to mention here the important findings of Raman spectroscopic studies including measurements of pore size, density and specific surface area on the densification of undoped...
SiO$_2$ gel as a function of heat treatment up to 900$^\circ$C [18]. With increasing temperature from 700 to 800$^\circ$C, the average pore size increases abruptly from 1.0 nm to 2.3 nm, whereas, the specific surface area decreases from 550 m$^2$/g to 160 m$^2$/g and the pore volume/gm decreases from 0.19 cc/g to 0.12 cc/g. The surface energy for a siloxane surface is higher than for a hydroxyl surface. The Si–OH groups condense to Si–O–Si bonds with increasing temperature, thus increasing the surface energy as well as enhancing pore collapse. In these rare earth elements doped gel-glass specimens, a large number of small pores collapse at 700$^\circ$C and an agglomeration of individual RE$^{3+}$ are set free after small pores collapse to form NPs. The remaining pores join to form larger pores. At still higher temperature (i.e., 800$^\circ$C), collapse of larger pores also takes place with similar observation in undoped sample, which is indicated by rapid fall of pore volume/g from 0.12 cc/g to 0.026 cc/g in going from 800$^\circ$C to 900$^\circ$C [18]. Thus it is possible at the highest temperature in the present case (i.e., 1200$^\circ$C), the rare earth oxide NPs grow to a maximum size because of complete annihilations of pores, leading to a disappearance of Si– OH groups to condensation of Si–O–Si bonds. To this end, we have systematically synthesized nano-glass composites systems with different doping concentrations of rare earth elements to prepare the sols, since the gelation process (rate of the hydrolysis and condensation reactions) strongly affect with varying the kind and/or the amount of the starting solvent and the final outcome of the preparation.

3. Experimental details

Powder X-ray diffraction (XRD) of the sample was performed by using Cu- $\kappa_a$ radiation. To analyze the detailed structure of samples, an ultrahigh-resolution transmission electron microscopy (TEM) (Model: JEM-3010, JEOL) was employed of NPs embedded SiO$_2$ glass matrix calcined at different temperatures. Impedance spectroscopic measurements with/without magnetic field are carried out in the temperature range 150–350 K using LCR meter (Model E4980A, Agilent) in conjunction with laboratory built cryostat arrangement integrated to the physical properties measurement system (Model: 6000, Quantum Design). The magnetization (zero-field-cooled and field-cooled conditions) and magnetic hysteresis measurements are performed using a SQUID magnetometer (Model: MPMS-XL, Quantum Design) with temperatures varying from 2 to 350 K with ±1.0 K thermal stability and equipped with a superconducting magnet producing fields up to ±60 kOe. The sample in the powder form was packed in polytetrafluoroethylene (PTFE) capsule, where sample mass was chosen in the range of 8 to 12 mg for obtaining a good signal-to-noise ratio. Room temperature extended X-ray absorption fine structure (EXAFS) experiments were carried out in fluorescence mode (very low concentration of RE$^{3+}$) at the RE ~ Er/Gd/La $L_{III}$-edge at the 17C beamline in the National Synchrotron Radiation Research Center (NSRRC), Hsinchu, Taiwan. The EXAFS analysis was based on a multiparameter single-scattering fit (by the FEFFIT code [19] and using standard IFEFFIT data analysis package) in the $R$-space from the first two coordination shells; the fitting in the $k$-space ($k^2$-weighted $\chi(k)$ with a $k$-cut range from 2.5-8 Å$^{-1}$) led to the same result. A reference sample of bulk RE$_2$O$_3$ (unsupported SiO$_2$ glass matrix) was used as a model standard for determining co-ordination numbers and inter-atomic distances. In obtaining the EXAFS
function $\chi(k)$, the background absorption features which were superimposed on the EXAFS oscillations were removed from the spectrum using spline fit to both the pre-edge and the post-edge regions.

4. Results and discussion

A. Structural studies through transmission electron microscopy (TEM) and X-ray diffraction (XRD): Typical data are shown for $\text{Er}_2\text{O}_3$:SiO$_2$ NPs-glass composite system having 0.5 mol% dopant $\text{Er}_2\text{O}_3$ concentration calcined at different temperatures, namely, 700, 800, 900, and 1200°C (henceforth referred as Er05-7, Er05-8, Er05-9 and Er05-12, respectively) [20]. Here, we discuss the TEM image of the powder specimen of typical Er05-8 (Figure 2(a)), showing nearly spherical NPs of $\text{Er}_2\text{O}_3$ embedded in the glass matrix in the range of 3–6 nm. The particle size distributions histogram (upper inset of Figure 2(a)) of the sample is calculated by counting onto the the micrograph at least 100 particles from Figure 2. The high-resolution TEM (HRTEM) image (lower inset of Figure 2(a)) of the respective sample also shows lattice fringes with interplanar spacing (3.04 Å). The selected area electron diffraction (SAED) pattern (Figure 2(b)) also shows spotted ring patterns, developing the regions of localized crystallinity.

![TEM image](image)

**Figure 2.** (Color online) (a) TEM image of Er05-8, upper inset: the particle size distribution histogram and lower inset: the HRTEM image, (b) electron diffraction and (c) XRD patterns of all the Er05-7, Er05-8 and Er05-12 samples.
The XRD patterns of the Er$_2$O$_3$ oxide NPs doped SiO$_2$ matrix calcined at 1200°C (Er05-12) show crystalline nature with quite large Er$_2$O$_3$ NPs. It exhibits clearly in Figure 2(c) the most intense characteristic line of single phase Er$_2$O$_3$ (JCPDF Card No. 43-1007) at 2θ ~ 29.30° (222) corresponding the unit cell parameter $a = 10.54$ Å (space group: $Ia3$ (206)). The sizes of Er-oxide NPs in Er05-12 are also estimated (> 40 nm) by applying the well-known Scherrer’s equation from the integral breadths of the XRD lines. XRD patterns cannot be well resolved from feeble broad peaks due to their amorphous-like character of Er05-7 and Er05-8 samples. However, it is significantly mentioned here that the sizes of Er$_2$O$_3$ NPs grow larger for samples calcined at higher temperatures. In the SiO$_2$ glass matrix, low concentrations of Er$^{3+}$ ions are bound to non-bridging oxygen atoms with quite low solubility [21]. Consequently, at a higher Er$_2$O$_3$ concentration with SiO$_2$ (1:2), the formation of an Er$_2$Si$_2$O$_7$ mixture with Er$_2$O$_3$ may occur at 1200°C [22]. However, at a higher calcined temperature (~1200°C and above), there is a possibility of the formation of Er$_2$Si$_2$O$_7$ mixture with crystalline Er$_2$O$_3$ even with very low concentration (0.5 mol %) of dopant ions. Herein, the sample obtained at 1200°C are not emphasized because of the observed dielectric behavior (discussed in the next section) is almost comparable with purebulk Er$_2$O$_3$ (unsupported with SiO$_2$).

B. Dielectric and magnetodielectric (MD) effect

Er$_2$O$_3$ NPs-glass composite system: colossal enhancement of dielectric constant and large MD effect

Among various rare earth oxides, Er$_2$O$_3$ has been chosen first in the present work as it possesses most appealing properties viz. high resistivity ($10^{12}$-$10^{15}$ cm$^{-3}$), large band gap ($E_g$ = 5–7 eV), static dielectric constant ($k$ ~ 14) [23,24], good thermodynamic stability with silicon and, moreover, not yet been explored from the viewpoint of observing the high MD effect. Although, present TEM and XRD studies also stimulate us for further exhaustive investigation on typical Er$_2$O$_3$:SiO$_2$ nano-glass composite system with different Er$_2$O$_3$ NPs size to throw more light exploring the origin and application feasibility on these rich dielectric materials. Typical data are shown for a Er$_2$O$_3$:SiO$_2$ nano-glass composite system having 0.5 mol% dopant (Er$_2$O$_3$) concentration calcined at different temperatures, namely, 700, 800, 900, and 1200°C (henceforth referred as Er05-7, Er05-8, Er05-9 and Er05-12 respectively).

4.1. Temperature dependence dielectric response

Figure 3(a) illustrates the relative dielectric constant ($\varepsilon'$) vs. temperature curves of typical Er05-8 sample without applied magnetic field measured at several selective frequencies (1–100 kHz). The shape of the curves with a notable broadening around the well-defined maxima $\varepsilon'_m$ (maximum value of $\varepsilon'$) is indicative of a diffuse phase transition (DPT) presence [25-27] with high $\varepsilon' (~ 600$ at $1$ kHz), quite different from and much higher than pure bulk Er$_2$O$_3$ ($\varepsilon' ~11.5$) [28] and SiO$_2$ ($\varepsilon' ~ 3.9$). Following the concept of DPT, the dielectric constant accords with a modified Curie–Weiss type equation viz. $\varepsilon' = \varepsilon'_m - \gamma(T - T_m)^\gamma$, where $\gamma$ is the diffuseness exponent indicative of degree of disorder, $C_i$ is a temperature independent coefficient (in general, dependent of frequency) and $\varepsilon'_m$ is the maximum value of $\varepsilon'$ at $T_m$. For $\gamma = 1$, normal Curie–Weiss behavior and $\gamma ~ 2$, it implies typical DPT for the ideal ferroelectric relaxor [29].
We obtained average $\gamma = 1.84$ from different slopes of linear fitting, which is close to the relaxor charge or interfacial polarization. The high dielectric value associated with DPT behavior diminished at different temperatures, inset shows ($\epsilon'$-$T$) curves of Er$_{0.5}$ nanoparticles doped SiO$_2$ glass calcined at different temperatures, inset shows ($\epsilon'$-$T$) curves of Er05-12 with respect to Bulk Er$_2$O$_3$ and SiO$_2$ showing non-DPT feature.

The plots of $\ln(\epsilon^{-1} - \epsilon_{m}^{-1})$ vs. $\ln(T - T_m)$ at several frequencies are illustrated in inset of Figure 3(a). We obtained average $\gamma = 1.84$ from different slopes of linear fitting, which is close to the relaxor value like other oxide relaxor systems [30]. The enhancement of dielectric value is observed even at temperatures below $T_m$ (~ 250–260 K), which ruled out the possibility of any space charge or interfacial polarization. The high dielectric value associated with DPT behavior (Figure 3(b)) diminishes with increasing calcined temperature (i.e., the Er$_2$O$_3$ NPs size). It is relevant to mention here that the temperature and frequency dependent dielectric phenomena of Er05-12 crystalline sample (calcined at 1200°C) without DPT behavior behaves like pure bulk Er$_2$O$_3$ [28] or SiO$_2$ glass (inset of Figure 3(b)). The critical calculation temperature above which DPT behavior completely diminishes for this typical concentration of Er$_2$O$_3$ (~ 0.5 mol %) is found to be around 1000°C. The DPT behavior is thus confined to the low temperature calcined (< 1000°C) system only where the NPs are in the 2–10 nm range.

4.2. Dielectric relaxation analysis

To shed more light on the relaxation dynamics of rare earth oxide NPs-glass composite systems, temperature dependent dielectric loss tangent ($\tan \delta$) are carried out at various frequencies. The appearance of three maxima with strong frequency dispersion located at peak $A$ ~180 K, peak $B$ ~260 K, and peak $C$ ~320 K are observed in $\tan \delta$ vs. temperature curve. The former two peaks (peaks $A$ and $B$) are shifted to high temperature with increasing frequency, whereas, the peak $C$ with high-dielectric leakage (~ 7) is shifted to the lower temperature. In Figure 4(b), the temperature dependence logarithmic plot of the relaxation time ($\tau$), determined as the inverse of the maximum peak frequency exhibit straight line, is shown in an Arrhenius representation $\tau = \tau_o \exp(E_{relax}/kT)$, with an energy barrier $E_{relax}$. Near the DPT temperature ($T_m$), thermally
activated response is described with an energy barrier $E_{\text{relax}}$ of about 1.13 eV. However, the temperature dependent relaxation response above 300 K becomes reversed with the activation energy 1.21 eV. These experimental facts suggest the presence of thermally activated oxygen vacancies associated with the dielectric relaxation process as presented earlier with activation energy $\sim$ 0.7-1.2 eV [30,31]. Our present results support the recent experimental finding of perovskite type ABO$_3$ [31] material, closely related to the thermally activated reorientation of dipole moment via the oxygen ion jumping through the oxygen vacancy, which can be controlled by sintering process. The dielectric response and DPT behavior diminishes with increasing calcined temperature (i.e., the high magnetic dilution of the NPs Er$_2$O$_3$ NPs size). It is relevant to mention here that the temperature and frequency dependent dielectric phenomena of Er$_05$-12 crystalline sample (calcined at 1200 $^\circ$C) without DPT behavior behaves like $\gamma$-Er$_2$O$_3$ glass matrix only where the NPs are in the 2–10 nm range.

Figure 5 shows the frequency and temperature dependence hysteresis loop ($P$-$E$ curves) of typical Er$_05$-8. The values of remanent polarization ($P_r$ $\sim$ 0.032 $\mu$C/cm$^2$) and coercive field ($E_c$ $\sim$ 0.78 kV/cm) of relatively narrow $P$-$E$ loop near $T_m$ (~270 K) without saturation are attributed to noncanonical ferroelectric-like (FEL) correlation in the sample, similar to those commonly observed in ABO$_3$ perovskites [32]. However, the present NP-glass composite system has very high magnetic dilution of the NPs Er$_2$O$_3$ concentration (0.5 mol% Er$_2$O$_3$ : 99.5 mol% SiO$_2$) and hence small amount of dipole moment per unit volume are not high enough to induce significant changes in the polarization. The spurious hysteresis loop reveals some contribution of lossy dielectric (space charge such as oxygen vacancies) or nicknamed as “banana loops,” the terminology recently coined by Scott [33]. At lower frequency, the hysteresis loop becomes slightly fatter. However, to check the possible FEL correlation in the sample, temperature
dependent $P$-$E$ characteristics are carried out at highest polarization frequency (2.0 kHz), obtained in our instrument (Precision LC meter, Radiant Technologies). It is noted that the measured hysteresis loop at high frequency is closely related with the intrinsic ferroelectric switching processes of the system [34]. Although, the values of remanent polarization and coercive field of $P$-$E$ curves becoming more pronounced with decreasing temperature from 320 to 275 K suggesting ferroelectric-like ordering in NPs-glass composite system, further investigations are certainly needed to delineate it.

4.4. Equivalent circuit analysis

Materials exhibiting colossal enhancement of dielectric value are usually adopted to explain by Maxwell–Wagner (MW) mechanism. The present NPs-glass composite system is basically NPs grain of rare earth oxide (uniformly distributed) embedded in more insulating SiO$_2$ matrix. The enhancement of dielectric constant along with DPT behavior might be a signature of the effect of internal barrier layer capacitance depending on the ration of grain size and the grain-boundary thickness. The complex impedance curves in Figure 6 have also been analyzed using an equivalent circuit, consisting of the two inclined semicircular arc (deviation from the ideal Debye response). Thus, the two depressed semi-arc in the Nyquist plot (complex impedance $Z''$-$Z'$ plane) of the impedance data could be modeled on two parallel resistor–capacitor (RC) networks connected in series, one corresponds to the conducting part in high frequency region assigned to the intrinsic effect of grain (typical Er$_2$O$_3$ NPs) and the other arc in low frequency side corresponds to the more resistive part (SiO$_2$ matrix) of the sample. Interestingly, the entire measured frequency region (20 – 2 × 10$^6$ Hz) at the temperature below $T_m$ (<270 K) is governed by the grain response (intrinsic effect). The temperature dependence of grain (Er$_2$O$_3$) resistance ($R_g$) values are obtained from equivalent circuit model with the help of commercial software (Z-VIEW, version 2.9c). The contribution of grain resistance (intrinsic

Figure 5. (Color online) Dielectric hysteresis loop of Er05-8, measured near DPT (275 K) and above room temperature (320 K) using 2.0 and 1.0 kHz polarization frequency.
The observation of colossal MD effect is the most interesting finding of Er05-8 system as shown in Figure 7(a) at a specific frequency of 2.5 kHz. The large enhancement of dielectric constant (~2.75 times) is observed around the transition regime 260–300 K under 9 T magnetic field. The inverse of dielectric constant with temperature under magnetic field (upper inset of Figure 7(a)) are also fitted by Curie–Weiss law with Curie constant (C) (3968.82, 6211.29 and 6918.04 K for 0, 5 and 9 T, respectively) and Curie–Weiss temperature (T_m) (260.06, 270.12 and 271.64 for 0, 5 and 9 T, respectively). It is obvious that both dielectric temperatures (T_m and T_o) are shifted to higher temperatures with increasing magnetic field, indicating the occurrence of magnetic spin-ordering at higher temperature under magnetic field and hence exhibit a reduced spin-lattice coupling strength under magnetic field. Temperature and frequency dependent dielectric constant of Er05-7 and Er05-8 are measured at a typical higher magnetic field (~9 T), shown in Figures 7(b) and 7(c). One may speculate about particle size dependent field effect playing a role of the larger ε’ response in the lower temperature annealed samples [35]. Within this scenario, the system in which we observed MD effect as well as Curie–Weiss behavior is the single phase of amorphous Er_2O_3 NPs of 2–10 nm size embedded in SiO_2 glass calcined at 700–900°C. The estimated field dependent MD response (MDR) near T_m (~275 K) is defined by \( \Delta \varepsilon / \varepsilon |_{H} \) (0%) = \( [\varepsilon(\epsilon(0)] / \varepsilon(0)] \times 100 \) as a function of the square of the magnetization as shown in the lower inset of Figure 7(a). Strikingly, the fractional change of the magnetic field induced change in the dielectric constant can be well approximated by the scaling function, \( \Delta \varepsilon / \varepsilon = \alpha M^2 \), where magnetoelastic interaction constant, \( \alpha \) is estimated at 0.782.

Figure 6. (Color online) (a) Complex plane plots, Z″-Z′, of Er05-8 at several temperatures and (b) schematic model of equivalent electrical circuits indicating of two parallel resistor–capacitor (RC) combinations \((R_gC_g, R_{gb}C_{gb})\) connected in series.
Similar behavior of the change in dielectric constant on the square of the magnetization is also observed in several materials including intrinsic multiferroics, such as BiMnO$_3$ [36], suggesting MD response in the present system (magnetic NPs of the guest oxide and SiO$_2$ host glass) are closely related to the magnetism, typical size and concentration of the Er$_2$O$_3$ NPs.

![Figure 7](image-url)

**Figure 7.** (Color online) (a) The magnetic field dependence of ($\varepsilon'$-T) curves of Er05-8 at a fixed frequency 2.5 kHz. Upper inset of (a): inverse of $\varepsilon'$ with temperature under magnetic field exhibiting the Curie–Weiss behavior and the lower inset of (a): the fractional change of the magnetic field induced change in the dielectric constant ($\Delta\varepsilon'/(\varepsilon'_0)$) of Er05-8 showing linear variation with the square of magnetization $M^2$, measured in the vicinity of $T_m$ ($\sim$ 275K). [(b), (c)] ($\varepsilon'$-T) curves of Er05-7 and Er05-8 samples measured with several selective frequencies under 9 T applied magnetic field.

### 4.6. Micro-structural correlated resistivity analysis

Figure 8 shows the contribution of amorphous NP Er$_2$O$_3$ grain resistance $R_g$ (calculated from equivalent circuit element analysis in Figure 6) of Er05-8 under external magnetic field as a function of measuring temperature. The temperature dependence of ac conductivity ($\sigma_{ac}$) at various frequencies is demonstrated in Figure 9. In the inset of Figure 9, the ac conductivity as a function of temperature under external magnetic field is illustrated. Concomitantly, the grain resistance $R_g(T)$ in Figure 8 exhibits a metal to insulator like transition coinciding with the dielectric maxima temperature $T_m$ of $\varepsilon'(T)$ (Figure 3(a)) as well as $\sigma_{ac}(T)$ (Figure 9). Interestingly, the $R_g$ decreases under magnetic field, similarly observed in colossal magnetoresistive
materials [25]. These experimental facts truely corroborate that the nature of charge carriers responsible for \textit{dc} conduction in the grain interior and the dielectric relaxation maxima belongs to the same category.

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure8.png}
\caption{Color online) Temperature dependence of grain resistance ($R_g$) calculated from impedance complex plane plots with external magnetic field. Inset: The region close to $T_m$ is highlighted.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure9.png}
\caption{(Color online) Temperature dependence of \textit{ac} conductivity ($\sigma_{ac}$) of Er05-8 for various frequencies. Inset: temperature dependence of \textit{ac} conductivity ($\sigma_{ac}$) at 2.5 kHz with external magnetic fields.}
\end{figure}

The magnetoresistive property of magnetic NPs is attributed by spin-polarized tunneling [37]. Although, the observed strong positive magnetoelectric interaction constant ($\alpha \sim 0.782$) has a similar appearance to intrinsic multiferroics, the MD effect can also be achieved through a combination of magnetoresistance and the Maxwell–Wagner effect, as predicted by Catalan.
Since the current results suggest that MD behavior is probably a manifestation of magnetoresistance changes, depending on the NP size and separation. Enhancement of MD response (i.e., positive MD effect) through the decreases of NPs Er$_2$O$_3$ resistance under external magnetic field, (i.e., negative magnetoresistance) might imply the possible tunability of the resistive MD effect.

Figure 10. (Color online) (a) The ($\varepsilon'$-$T$) curves of Eu05-8 at different frequency, inset: representative plots of $\ln(\varepsilon'^{-1}-\varepsilon'^{-1}_m)$ vs $\ln(T-T_m)$ at temperatures higher than $T_m$ for the Eu05-8 at different frequency values.

Figure 11. (Color online) (a), (b) The ($\varepsilon'$-$T$) curves of Eu05-7 and Eu05-9 measured under different applied magnetic fields at a fixed frequency 2.5 kHz.
5. Eu₂O₃ NPs-glass composite system: Smaller dielectric response and negative MD effect

Typical data is shown for Eu₂O₃:SiO₂ NPs-glass composite system having 0.5 mol% dopant Eu₂O₃ concentration calcined at different temperatures, namely, 700, 800 and 900°C (henceforth referred as Eu05-7, Eu05-8 and Eu05-9 respectively). Figure 10 represents the temperature dependence of ε′ of Eu05-7 in the absence of the magnetic field. The nature of the variation of the (ε′-T) curves with maxima at T_m ∼ 270 K, represents as “diffuse phase transition” (DPT) around T_m with smaller ε′ than Er05-7 system, quite different and larger than that of bulk Eu₂O₃ [28] or pure SiO₂ (∼ 3.9). Such system also follows a modified Curie–Weiss relationship [29], obtaining diffuseness exponent γ =1.58 (inset of Figure 10). The ε′-T plot (at 2.5 kHz), around the transition regime 240-320 K of Eu05-7 and Eu05-9 shows a decrease of ε′ under a magnetic field of 9 T (Figure 11). Here, we also observed particle size dependent effect, associated with DPT behavior as well as MD effect.

6. Effect of different rare earth oxides on the dielectric properties

In previous sections, we have presented interesting particle size dependent colossal dielectric response along with MD effect in Er₂O₃ and Eu₂O₃ nano-glass composite systems. From the obtained results, there are colossal enhancement of dielectric constant and large MD effect in Er₂O₃ case [20], while those in Eu₂O₃ case, smaller responses were observed [39]. Obviously, the different electronic and magnetic properties for Er₂O₃ and Eu₂O₃ play a crucial role. However, these results suggest great promise in further systematic investigation to distinguish the mechanisms that contribute to colossal dielectric responses along with MD effect in other RE₂O₃:SiO₂ nano-glass composite systems (RE₂O₃, RE ~ rare earth, a series of elements from La to Lu with stable RE³⁺) with different RE₂O₃ NPs size. The purpose of such study is to find amorphous high-k oxide candidates and MD effect with superior phase stability for gate dielectrics from a lineup of rare earth metal oxides embedded in SiO₂ matrix, and to find a sequential coupling between different constituents among these nano-glass composite materials.

Figure 12 illustrates the temperature dependent ε′ of the series of rare earth oxide NPs-glass composite systems calcined at 700°C in the absence of the magnetic field. Here, we concentrate the variations of temperature dependent dielectric behavior mainly on the 700°C calcined sample for the sake of clarity. Besides that, the possibility of formation of other rare earth oxide phase (e.g., RE₂Si₂O₇) mixture with crystalline RE₂O₃ is ruled out at 700°C for low dopant concentration (0.5 mol%) [22]. Interestingly, RE₂O₃:SiO₂ nano-glass composite systems in which RE ~ Sm, Gd and Er show colossal enhancement of dielectric constant (ε′ ~10⁴) around room temperature. The nature of the variation of the (ε′-T) curves represents well-defined maxima and notable dielectric broadening around ε′ m (maximum value of ε′) with high ε′ and different from pure bulk RE₂O₃.
Figure 12. (Color online) The $\varepsilon'$-T curves of RE$_2$O$_3$ (gel-glass calcined at 700°C) at 1 kHz without applied magnetic field.

Figure 13. (Color online) (a) Maximum value of dielectric constant, and (b) MDR under 5 T applied field of RE$_2$O$_3$:SiO$_2$ nano-glass composite systems calcined at 700°C with rare earth atomic number.
The amorphous self-organized rare earth oxide nano-glass composite systems may be the promising high-$k$ gate dielectrics due to its reproducible high dielectric constant (Figure 13(a)), single-stage process in air at moderate temperature and good compatibility with modern microelectronics processing technique. The present systems also show the MD effect around the transition temperature. The MDR at 1 kHz is plotted as a function of atomic number of the rare earth elements near $T_m$ as shown in the Figure 13(b). The RE$_2$O$_3$:SiO$_2$ nano-glass composite systems in which RE ~ Sm, Gd, Er and Lu show colossal response of dielectric constant under applied magnetic field. Sol–gel process provides a convenient way for tailoring phase pure, self-organized NPs of nearly uniform sizes (particle size distribution histogram from TEM image) and for facilitating homogeneous dispersion of these metal-oxide NPs in the silica matrix. It is believed that the sol–gel derived NP-glass composite systems prepared and calcined in identical condition (Figure 1(b)), the particle size distributions of all rare earth oxide at specific calcined temperature is nearly equal (say 700°C, we have checked for Er, Eu, Gd and La systems). These rare earth oxide NPs are rigidly fixed within the insulating silica matrix at all temperatures. So this dielectric behavior does not arise from the physical motion of the NPs. This feature takes place inside the rare earth NPs grain and they are very much conditioned by magnetic property of NPs grain, the potential barriers in the grain boundaries, the degree of deformation of the lattice and the crystallites, as well as the grain size and their constituent host. Why RE ~ Sm, Gd and Er shows much larger effects than other rare earths? It needs further investigation using magnetic and non-magnetic rare earth oxide NPs together with different doping concentrations to explore the mechanism and application feasibility on these rich dielectric materials.

7. Effect of molar concentration of magnetic NPs on the observed dielectric and MD properties

As discussed in the above section, we have systematically investigated the colossal responses of dielectric behavior along with MD effect in rare earth oxide (RE$_2$O$_3$, RE ~ rare earth, a series of elements from La to Lu with stable RE$^{3+}$) NPs embedded SiO$_2$ glass composite systems with different RE$_2$O$_3$ NPs size. Properly annealed NPs-glass composites, where RE ~ Sm, Gd and Er, show an intriguing colossal response of dielectric behavior and MD effect near room temperature. These reproducible experimental facts suggest simultaneously a question why only these three magnetic rare earth elements have larger effects than others. Herein, we have systematically synthesized together via sol–gel route the magnetic Gd$_2$O$_3$ and non-magnetic La$_2$O$_3$ NPs with different doping concentrations and size embedded in SiO$_2$ matrix. The doping concentration and the corresponding sample index are highlighted in Table II [40]. Here, we report that the high-$k$ and MD of these NP-glass composite systems are very much conditional by magnetic property of Gd$_2$O$_3$ NPs size, concentration, and the degree of deformation of the host matrix. To improve the dielectric tunability in presence of external magnetic field, the crucial magnetic properties of dielectrics are necessary for the application of the devices.
Table 2. Different doping concentrations of non-magnetic La$_2$O$_3$ and magnetic Gd$_2$O$_3$ (mol%) in SiO$_2$ NP-glass composite systems.

| Sample name | Non-magnetic La$_2$O$_3$ (mol%) | Magnetic Gd$_2$O$_3$ (mol%) |
|-------------|---------------------------------|-----------------------------|
| LGS1        | 0.150                           | 0.000                       |
| LGS2        | 0.120                           | 0.030                       |
| LGS3        | 0.090                           | 0.060                       |
| LGS4        | 0.075                           | 0.075                       |
| LGS5        | 0.060                           | 0.090                       |
| LGS6        | 0.000                           | 0.150                       |
| LGS7        | 0.000                           | 0.500                       |

Figure 14 illustrated the $\varepsilon'$-$T$ curves of La$_2$O$_3$/Gd$_2$O$_3$ NPs embedded SiO$_2$ glass composite systems (henceforth referred to as LGS) with different doping concentrations in the absence of the magnetic field. All the curves have well-defined diffuse phase transition-like maxima at $T_m \approx 320$ K characteristic with oxygen vacancy-induced dielectric relaxation, thoroughly discussed in our previously reported sections [16,20,39] of other rare earth systems. Interestingly, at higher magnetic Gd$_2$O$_3$ doping concentrations, the LGS NP-glass composite systems show colossal enhancement of dielectric behavior near room temperature. Even, a very high magnetic dilution of Gd$_2$O$_3$ NPs (LGS2 sample ~ doping level 0.03 mol%) system, the dielectric value is higher than that of pure bulk crystalline counterpart [28].

![Figure 14](image-url)
Figure 15(a) illustrates the $\varepsilon^{\prime}_{\text{max}}$ vs. Gd$_2$O$_3$ doping concentrations of NP-glass composite systems calcined at 700°C in the absence of the magnetic field. Here, $\varepsilon^{\prime}_{\text{max}}$ increases with higher doping concentration of magnetic Gd$_2$O$_3$ NPs. The present systems also show strong MDR around the transition temperature ($T_m$). The MDR at several selective frequencies near $T_m$ are plotted as a function of doping concentration of Gd$_2$O$_3$ shown in the Figure 15(b). MDR enhances with faster rate at relatively lower doping concentration ($\leq$0.1 mol%) of magnetic Gd$_2$O$_3$, whereas at moderate concentration range ($\geq$0.2 mol%), the colossal response are more pronounced. A profound analogy may be expected between the colossal MDR in magnetic NP-glass composite systems and the inhomogeneous magnetoelectric interaction, inducing through magnetic spin modulation (flexomagnetoelectric polarization) [41]. Depending on the characteristic size (particle radius) and magnetization in amorphous-like nanosized systems, the flexomagnetoelectric effect induces linear magnetoelectric tunability [42].

Figure 15. (Color online) (a) Maximum value of dielectric constant, and (b). MDR under 5 T applied field of LGS NP-glass composite systems with different Gd$_2$O$_3$ doping concentrations calcined at 700°C.

8. Extended X-ray Absorption Fine Structure (EXAFS) experiments

Extended X-ray absorption fine structure (EXAFS) experiments were performed at the Gd $L_{\text{III}}$ edge to obtain further detailed information on the local surroundings of the chemical elements of the Gd-oxide doped (0.5 mol%) nano-glass composite system calcined at different temperatures, namely, 700, 800, 900, and 1200°C (henceforth referred as Gd05-7, Gd05-8, Gd05-9, and Gd05-12, respectively). The broad dielectric anomaly in Gd$_2$O$_3$:SiO$_2$ can be plausibly attributed to oxygen vacancy defects, which are implied by the EXAFS measurements. Of particular interest are the coordination number of oxygen around the Gd atom and type of neighbors,
the interatomic distance between the Gd atom and the surrounding oxygen, and the Debye–Waller factors which contain the mean-square relative displacements due to static disorder or thermal vibration. Figure 16 depicts the room temperature experimental EXAFS spectra of samples Gd05-7, Gd05-8 and Gd05-9. The EXAFS signals weighted by \( k^2 \) [i.e., \( k^2\chi(k) \)] are shown in Figure 16(a), and the moduli of their Fourier transforms \( |F(R)| \) are presented in Figure 16(b). The EXAFS spectra in Figure 16(a) look very much the same, on the first glance, and thus one would not expect a major difference in the Fourier transform data. The Fourier transform modulus (Figure 16(b)) exhibits two main coordination peaks: the first one, located at \( R \sim 1.8 \) Å corresponds to the interatomic distances of Gd\(^{3+}\)–O (first coordination shell), while the second one (not growing properly) is located at \( R \sim 2.8 \) Å, indicating mostly the amorphous environment of Gd [21], as expected for a Gd–Gd coordination (second coordination shell) in a crystal. However, the TEM results confirm the presence of NPs Gd\(_2\)O\(_3\) with localized crystallinity in the glass specimen calcined at 700°C. The fitting results of Gd\(^{3+}\)–O interatomic distances obtained from Figure 16 are summarized as a function of calcination temperatures in Table III. The values obtained from the EXAFS spectra are not significantly different in all the glass specimens with very low doping concentration. However, on close inspection it is evident that the average Gd\(^{3+}\)–O interatomic distance of Gd05-7 is shorter than that of Gd05-8, Gd05-9, and bulk Gd\(_2\)O\(_3\) (unsupported SiO\(_2\) glass matrix), suggesting that oxygen ions surrounding the oxygen vacancies around Gd ions should concurrently involve a relaxation toward their adjacent vacancies and, as a result, shorter bond length can be attributed [43]. This argument can, presumably, also be applied to the Er\(_2\)O\(_3\)–SiO\(_2\) NP-glass system. It has been found that the porous glass are formed at \( \sim 400°C \) and annihilation of pores start at \( \sim 700°C \), completed at \( \sim 800°C \) [44]. Therefore, silica gel-glass doped with low concentration of rare earth ions are subjected to systematic heating, the collapse of the silica pores is initiated near 700°C (Si–OH groups condense to Si–O–Si bonds). In this calcined glass, agglomeration of individual rare earth oxide ions loosely attached to the pores to be detached to form clusters. The dimensions of the clusters reside in the nanometer range. At 700°C calcined sample, in rare earth oxide NPs, oxygen vacancies could be easily created by loss of oxygen at low oxygen partial pressure, according to \( O_2 \rightarrow V_0 + 1/2 O_2 \). Based on these considerations, the formation of oxygen vacancies inside the NPs influence the bond-length change, and the number of oxygen atoms surrounding the Gd atom should also decrease. This argument is in fair agreement with the result of a relative decrease in the number of nearest neighbors (Table III) in Gd05-7 in comparison with other high temperature calcined samples. At higher temperature, namely, 800°C, collapse of larger pores also takes place, agglomerate more RE\(_2\)O\(_3\) to form bigger size NPs [18]. This implies that annealing at higher temperatures increase the particle size with lower \( V_0 \) concentration. These results are consistent with dielectric studies, resulting in the decrease in dielectric constant along with DPT behavior by annealing the sample at higher temperatures. Likewise, the Debye-Waller factor increases with decreasing NPs size, indicating that the disorder in oxygen environment increases with lower calcination temperatures. In this connection, it is relevant to refer to the important findings of RE\(^{3+}\) doped EXAFS studies by Rocca et al. [45] on the densification of silica xerogels as a function of heat treatment up to 900°C. Their measurements have shown that the densification of xerogel without evidence of clustering of RE\(^{3+}\) induces a decreasing of the co-ordination number and a shortening of the
The transformation range is correctly, the oxygen vacancy) for which further experiments of all the rare earth with different coordination number with lower calcined nano-glass specimens depends on NPs size (or, more main RE–O distance and absence of RE–RE correlation. Nevertheless, our TEM studies in densified glass specimens (700°C and above) have revealed clear detectable NPs with separation. So, it is reasonable to assume that the shortening of Gd3+-O and the decreasing of the coordination number with lower calcined nano-glass specimens depends on NPs size (or, more correctly, the oxygen vacancy for which further experiments of all the rare earth with different doping concentrations are still necessary. Therefore, our EXAFS findings provide additional insight into the origin of the unusually colossal room-temperature dielectric response in rare earth oxide NPs embedded oxide glasses.

| Sample     | Bond type            | EXAFS              |
|------------|----------------------|--------------------|
|            |                      | $N$                |
| Gd05-7     |                      | 5.3±0.2            |
| Gd05-8     | First coordination shell | 5.6±0.2            |
| Gd05-9     | (Gd3+-O)             | 5.8±0.3            |
| $\text{Gd}_2\text{O}_3$ |                    | 6.0±0.2            |

Table 3. Results of the quantitative analysis of the first coordination shell derived from EXAFS filtered data of Gd$_2$O$_3$:SiO$_2$ nano-glass composite systems at different calcinations temperatures. $N$, $R$ and $\sigma^2$ are the average coordination number, interatomic distance, and relative mean square displacement (Debye-Waller factor), respectively.

Figure 16. (Color online) Gd $L_{\text{III}}$-edge EXAFS spectra of Gd$^{3+}$-doped SiO$_2$ glass samples calcined at different temperatures. Spectra are vertically shifted for clarity. (a) $k^2$-weighted EXAFS signals. (b) Fourier transforms moduli radial distribution functions. Both experimental data (symbols) and the best-fit theoretical curves (dashed) are also reported. The transformation range is $k = 2.5-8$ Å$^{-1}$ for all the spectra and the range for the first coordination shell fit is $R = 1-3$ Å.

Figure 17 depicts the room temperature experimental EXAFS spectra of LGS systems ((La, Gd)$_2$O$_3$:SiO$_2$ NP-glass composite systems) with different doping concentrations (Table II) and
particles size (different calcined temperatures). The first coordination peak located at ~1.8 Å (Figures 17(a), (b)) with the interatomic distance of La\(^{3+}\)-O/Gd\(^{3+}\)-O looks very much the similar without any perceptible shift at different doping concentrations. However, the interatomic distances of the first coordination peak (~1.8 Å) of LGS4 with different calcination temperatures (Figures 17(c), (d)) are shifted significantly even with very low doping concentration of La\(_2\)O\(_3\)/Gd\(_2\)O\(_3\). It reveals significantly that the average La\(^{3+}\)-O/Gd\(^{3+}\)-O interatomic distances of LGS4 samples at lower calcination temperature is shorter, suggesting higher oxygen vacancies around La/Gd ions, supported with our previously reported article [16]. Therefore, the dielectric value decreases by annealing the sample at higher temperatures (or, more correctly, with higher NPs size) with identical molar concentration of dopant element. However, identical particle size (magnetic and/or non-magnetic NPs) with concentration dependence does not affect the oxygen vacancies. In other words, oxygen vacancies depend only on the particle size but not its magnetic phase.

![Figure 17](image_url)

**Figure 17.** (Color online) Room temperature Fourier transforms moduli radial distribution functions EXAFS spectra of LGS systems at (a) La \(L_{\text{III}}\)-edge with different La\(_2\)O\(_3\) concentrations, (b) Gd \(L_{\text{III}}\)-edge with different Gd\(_2\)O\(_3\) concentrations calcined at 700\(^\circ\)C, (c) La \(L_{\text{III}}\)-edge of LGS4 sample at different calcined temperatures, and (d) Gd \(L_{\text{III}}\)-edge of LGS4 sample at different calcined temperatures. Spectra are vertically shifted for clarity.

9. Magnetic measurements

The \(dc\) magnetization (after diamagnetic correction) of LGS5 sample under zero-field-cooled (ZFC) and field-cooled (FC) condition as a function of temperature (2–350 K temperature
range) in the presence of an applied magnetic field of 200 Oe are shown in Figure 18. It is noteworthy that the observed temperature dependent magnetic feature of LGS5 sample is attributed from magnetic transition of Gd$_2$O$_3$ NPs only. On close inspection, the divergent behavior between ZFC and FC data occurs at low temperatures (irreversibility temperature, $T_{\text{irr}}$) with a rounded maximum for ZFC curve is obtained at 58 K (identified as the blocking temperature, $T_B$). A spread in the blocking temperature may be rightly assumed with NPs size distribution. Such behavior is akin to superparamagnetic phase of Gd$_2$O$_3$ NPs in the nano-glass composite system similarly observed in oxide glasses containing Gd$_2$O$_3$ [46]. This typical characteristic temperature would be unlikely arising from a magnetic transition in oxygen contaminant [47]. The FC magnetization increases continuously with the lowering of temperature below the irreversibility temperature, consistent with ferromagnetic-like ordering of Gd$_2$O$_3$ NPs. The shape of the inverse susceptibility data (right axis of Figure 18) reveal a quite different behavior in comparison with usually found Curie-type behavior in bulk Gd$_2$O$_3$ [48].

![Figure 18](image-url)  
**Figure 18.** (Color online) ZFC and FC magnetization versus temperature curves of LGS5 sample calcined at 700°C, right axis shows the temperature dependent inverse susceptibility curve. In the inset, the region close to the superparamagnetic transition is highlighted.

The data obtained for the temperature dependence magnetization of LGS4 samples calcined at 700, 800, 900 and 1200°C are graphically depicted in Figure 19. The superparamagnetic blocking temperature cannot be traced in low accuracy (or resolution) of measurement with very low percentage-doping (~ 0.075 mol%) of magnetic Gd$_2$O$_3$. However, from the observed continuous increase in ZFC and FC curves at low temperature indicating the ferromagnetic nature of the LGS4 sample. Magnetic properties with size dependency are also observed for LGS4 samples calcined at different temperatures, related with the uncompensated surface spins present on the Gd$_2$O$_3$ NPs. It is likely that the Gd$_2$O$_3$ NPs with smaller size (i.e., higher surface-to-volume ratio) contain larger proportion of uncompensated surface spins and
This constitutes strong evidence that at 5 K the Gd NPs are best described as an assembly of non-interacting superparamagnetic NPs. The hysteresis curves have no magnetic saturation in the magnetic field range of ±60 kOe, considering large anisotropic fields appears in the Gd$_2$O$_3$ NPs systems [49].

 Isothermal magnetization-field sweeps were performed to further investigate the nature of the superparamagnetic state and the ferromagnetism below transition temperature. Figure 21 displays the magnetic field dependence of the magnetization ($M$-$H$) curves for LGS4 sample calcined at 700°C at 300, 200, 100 and 5 K in the dc magnetic field range ±60 kOe. Defining the magnetic characteristics, magnetic hysteresis curve obtained at 300 K has zero area, whereas, there is a dramatic change both in magnitude (enhancement of magnetic moment/unit mass) and shape (deviate from linearity) with measurable finite areas at 5 K (lower inset of Figure 21). This constitutes strong evidence that at 5 K the Gd$_2$O$_3$ NPs are going to the magnetically ordered state or in ferromagnetic nature. Moreover, magnetization vs $H/T$ curves plotted at different temperatures are linear and collapse to a single curve (upper inset of Figure 21) confirming the existence of superparamagnetic phase of Gd$_2$O$_3$ NPs embedded in SiO$_2$ glass matrix. It is abundantly clear that Gd$_2$O$_3$ NPs grown with high magnetic dilution in glass matrix are best described as an assembly of non-interacting superparamagnetic NPs. The hysteresis curves have no magnetic saturation in the magnetic field range of ±60 kOe, considering large anisotropic fields appears in the Gd$_2$O$_3$ NPs systems [49].

Figure 19. (Color online) ZFC and FC magnetization versus temperature curves of LGS4 sample at different calcination temperatures. Applied dc magnetic field 200 Oe.

consequently reveal higher ferromagnetic values than larger NPs (higher calcined temperature). Temperature dependent inverse susceptibility data for LGS4 samples calcined at different temperatures with respect to bulk Gd$_2$O$_3$ can be fitted by the Curie–Weiss law (Figure 20(a)) having different slopes of straight lines. The intersection points of fitted lines with x-axis exhibit the Curie–Weiss temperatures, found to be 32.7, 16.6, 12.1 and 4.8 K for 700, 800, 900 and 1200°C respectively. These positive values for LGS4 sample calcined at different temperatures indicate weak ferromagnetic behavior, whereas, bulk Gd$_2$O$_3$ shows antiferromagnetism with negative Curie–Weiss temperature at -16.3 K. The current tendency of lowering Curie-Weiss temperatures with increasing calcined temperature for LGS4 samples infers that larger sized Gd$_2$O$_3$ NPs possess toward bulk crystalline counterpart.

Isothermal magnetization-field sweeps were performed to further investigate the nature of the superparamagnetic state and the ferromagnetism below transition temperature. Figure 21 displays the magnetic field dependence of the magnetization ($M$-$H$) curves for LGS4 sample calcined at 700°C at 300, 200, 100 and 5 K in the dc magnetic field range ±60 kOe. Defining the magnetic characteristics, magnetic hysteresis curve obtained at 300 K has zero area, whereas, there is a dramatic change both in magnitude (enhancement of magnetic moment/unit mass) and shape (deviate from linearity) with measurable finite areas at 5 K (lower inset of Figure 21). This constitutes strong evidence that at 5 K the Gd$_2$O$_3$ NPs are going to the magnetically ordered state or in ferromagnetic nature. Moreover, magnetization vs $H/T$ curves plotted at different temperatures are linear and collapse to a single curve (upper inset of Figure 21) confirming the existence of superparamagnetic phase of Gd$_2$O$_3$ NPs embedded in SiO$_2$ glass matrix. It is abundantly clear that Gd$_2$O$_3$ NPs grown with high magnetic dilution in glass matrix are best described as an assembly of non-interacting superparamagnetic NPs. The hysteresis curves have no magnetic saturation in the magnetic field range of ±60 kOe, considering large anisotropic fields appears in the Gd$_2$O$_3$ NPs systems [49].

Figure 19. (Color online) ZFC and FC magnetization versus temperature curves of LGS4 sample at different calcination temperatures. Applied dc magnetic field 200 Oe.
10. Conclusions

We have synthesized self-organized RE$_2$O$_3$ NPs with almost equal size and separation embedded in SiO$_2$ glass matrix by the sol–gel method.

Principal findings may be summarized below:

Figure 20. (Color online) (a) Inverse susceptibility versus temperature curves of LGS4 samples at different calcination temperatures with respect to bulk Gd$_2$O$_3$, (b) the region close to the extrapolated lines intersect with temperature axis is highlighted.

Figure 21. (Color online) Hysteresis loop of LGS4 sample calcined at 700°C, lower inset: the region close to the coercive field value is highlighted, upper inset: magnetization vs. H/T of LGS4 sample.
a. Presence of superparamagnetic phase occurs in magnetic rare earth oxide NPs doped glass samples.

b. Properly annealed sol–gel glass (in which RE ~ Sm, Gd and Er) (Fig. 2) shows an interesting colossal response of dielectric constant along with DPT and MD behavior around room temperature.

c. The experimental facts strongly suggest that the dielectric anomaly with DPT behavior is related to oxygen vacancy-induced dielectric relaxation in the material without ferroelectric phase transition.

d. The MDR observed in this glassy composite is considered to be associated with the direct consequence of magnetoresistance changes depending on the calcination temperatures (magnetic NPs size).

e. However, keeping the NPs size constant, the increase in dielectric constant and MDR strongly depends on the magnetic property (superparamagnetism) of the rare earth ions.

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References

[1] Chau R, Datta S, Doczy M, Doyle B, Kavalieros J, Metz M. High-k/Metal gate stack and its MOSFET characteristics. IEEE Electron Device Lett 2004;25:408–10.
[2] Lo SH, Buchanan DA, Taur Y, Wang W. Quantum-mechanical modeling of electron tunneling current from the inversion layer of ultra-thin-oxide MOSFETs. IEEE Electron Device Lett 1997;18:209–11.

[3] Homes CC, Vogt T, Shapiro SM, Wakimoto S, Ramirez AP. Optical response of high-dielectric-constant perovskite-related oxide. Science 2001;293:673–6.

[4] Liu J, Duan CG, Yin WG, Mei WN, Smith RW, Hardy JR. Large dielectric constant and Maxwell-Wagner relaxation in Bi$_{2/3}$Cu$_3$Ti$_4$O$_{12}$. Phys Rev B 2004;70:144106(7).

[5] Martin SG, Orrantia AM, Aguirre MH, Franco MÁA. Giant barrier layer capacitance effects in the lithium ion conducting material La$_{0.67}$Li$_{0.25}$Ti$_{0.75}$Al$_{0.25}$O$_3$. Appl Phys Lett 2005;86:043110(3).

[6] Yang Z, Hou Y, Liu B, Wei L. Structure and electrical properties of Nd$_2$O$_3$-doped 0.82Bi$_{1/3}$Na$_{1/3}$TiO$_3$–0.18Bi$_{1/3}$K$_{1/3}$TiO$_3$ ceramics. Ceram Int 2009;35:1423–7.

[7] Wang Z, Chen XM, Ni L, Liu XQ. Dielectric abnormalities of complex perovskite Ba(Fe$_{1/2}$Nb$_{1/2}$)O$_3$ ceramics over broad temperature and frequency range. Appl Phys Lett 2007;90:022904(3).

[8] Raevski IP, Prosandeev SA, Bogatin AS, Malitskaya MA, Jastrabik L. High dielectric permittivity in AFe$_{1/2}$B$_{1/2}$O$_3$ nonferroelectric perovskite ceramics (A=Ba, Sr, Ca; B=Nb, Ta, Sb). J Appl Phys 2003;93:4130–6.

[9] Wu JB, Nan CW, Lin YH, Deng Y. Giant dielectric permittivity observed in Li and Ti doped NiO. Phys Rev Lett 2002;89:217601(4).

[10] Pecharromán C, Esteban-Betegón F, Bartolomé JF, López-Esteban S, Moya JS. New percolative BaTiO$_3$–Ni composites with a high and frequency-independent dielectric constant (e$_r$ ≈ 80 000). Adv Mater 2001;13:1541–4.

[11] Cohn JL, Peterca M, Neumeier JJ. Low-temperature permittivity of insulating perovskite manganites. Phys Rev B 2004;70:214433(6).

[12] Park T, Nussinov Z, Hazzard KRA, Sidorov VA, Balatsky AV, Sarrao JL, Cheong SW, Hundley MF, Lee JS, Jia QX, Thompson JD. Novel dielectric anomaly in the hole-doped La$_2$Cu$_{1-x}$Li$_x$O$_4$ and La$_{2-x}$Sr$_x$NiO$_4$ insulators: signature of an electronic glassy state. Phys Rev Lett 2005;94:017002(4).

[13] Rivas J, Rivas-Murias B, Fondado A, Mira J, Señarís-Rodríguez MA. Dielectric response of the charge-ordered two-dimensional nickelateLa$_{1.5}$Sr$_{0.5}$NiO$_4$. Appl Phys Lett 2004;85:6224–6.

[14] Zhu WJ, Tamagawa T, Gibson M, Furukawa T, Ma TP. Effect of Al inclusion in HfO$_2$ on the physical and electrical properties of the dielectrics. IEEE Electron Device Lett 2002;23:649–651.
[15] Mukherjee S, Pal AK, Bhattacharya S, Raittila J. Magnetism of Mn$_2$O$_3$ nanocrystals dispersed in a silica matrix: Size effects and phase transformations. Phys Rev B 2006;74:104413(10).

[16] Mukherjee S, Lin YH, Kao TH, Chou CC, Yang HD. Searching for high-k RE$_2$O$_3$ nanoparticles embedded in SiO$_2$ glass matrix. J Appl Phys 2012;111:064103(6).

[17] Sakka S, Kamiya K. The sol–gel transition in the hydrolysis of metal alkoxides in relation to the formation of glass fibers and films. J Non-Cryst Solids 1982;48:31–46.

[18] Krol DM, van Lierop JG. The densification of monolithic gels. J Non-Cryst Solids 1984;63:131–44.

[19] Ankudinov A, Ravel B, Rehr JJ, Newville M. FEFFIT Manual within the FEFF Project (Seattle, WA: University of Washington, USA); 1992–1999.

[20] Mukherjee S, Chen CH, Chou CC, Tseng KF, Chaudhuri BK, Yang HD. Colossal dielectric and magnetodielectric effect in Er$_2$O$_3$ nanoparticles embedded in a SiO$_2$ glass matrix. Phys Rev B 2010;82:104107(7).

[21] Afify ND, Dalba G, Kuzmin A. Local structure around Er$^{3+}$ in SiO$_2$-HfO$_2$ glassy waveguides using EXAFS. Phys Rev B 2007;76:024114(8).

[22] Maqsood A. Phase transformations in Er$_2$Si$_2$O$_7$ ceramics. J Mater Sci Lett 1997;16:837–840.

[23] Losurdo M, Giangregorio MM, Capezzuto P, Bruno G, Malandrino G, Fragalà IL, Armelao L, Barreca D, Tondello E, Suvorova AA, Yang D, Irene EA. Multifunctional nanocrystalline thin films of Er$_2$O$_3$: interplay between nucleation kinetics and film characteristics. Adv Funct Mater 2007;17:3607–12.

[24] Chen S, Zhu YY, Xu R, Wu YQ, Yang XJ, Fan YL, Lu F, Jiang ZM, Zou J. Superior electrical properties of crystalline Er$_2$O$_3$ films epitaxially grown on Si substrates. Appl Phys Lett 2006;88:222902(3).

[25] Rivas J, Mira J, Rivas-Murias B, Fondado A, Dec J, Kleemann W, Señarís-Rodríguez MA. Magnetic-field-dependent dielectric constant in La$_{2/3}$Ca$_{1/3}$MnO$_3$. Appl Phys Lett 2006;88:242906(3).

[26] Jana A, Kundu TK, Pradhan SK, Chakravorty D. Dielectric behavior of Fe-ion-doped BaTiO$_3$ nanoparticles. J Appl Phys 2005;97:044311(6).

[27] Rivera I, Kumar A, Ortega N, Katiyar RS, Lushnikov S. Divide line between relaxor, diffused ferroelectric, ferroelectric and dielectric. Solid State Commun 2009;149:172–6.

[28] Lal HB. Low temperature dielectric studies of some rare-earth oxides. J Phys C: Solid State Phys 1980;13:3969–76.
[29] Yu Z, Ang C, Guo R, Bhalla AS. Ferroelectric-relaxor behavior of Ba(Ti$_{0.7}$Zr$_{0.3}$)O$_3$ ceramics. J Appl Phys 2002;92:2655–7.

[30] Raymond O, Font R, Suárez-Almodovar N, Portelles J, Siqueiros JM. Frequency-temperature response of ferroelectromagnetic Pb(Fe$_{1/2}$Nb$_{1/2}$)O$_3$ ceramics obtained by different precursors. Part I. Structural and thermo-electrical characterization. J Appl Phys 2005;97:084107(8).

[31] Ang C, Yu Z, Cross LE. Oxygen-vacancy-related low-frequency dielectric relaxation and electrical conduction in Bi: SrTiO$_3$. Phys Rev B 2000;62:228–36.

[32] Samara GA. The relaxational properties of compositionally disordered ABO$_3$ perovskites. J Phys: Condens Matter 2003;15:R367–R411.

[33] Scott JF. Ferroelectrics go bananas. J Phys: Condens Matter 2008;20:021001(2).

[34] Pintilie L, Alexe M. Ferroelectric-like hysteresis loop in nonferroelectric systems. Appl Phys Lett 2005;87:112903(3).

[35] Yáñez-Vilar S, Mira J, Sánchez-Andújar M, Castro-García S, Fondado A, Rivas J, Senarís-Rodríguez MA. Particle size reduction: a way to enhanced dielectric properties of magnetocapacitive La$_{2/3}$Ca$_{1/3}$MnO$_3$. Appl Phys Lett 2010;96:162904.

[36] Kimura T, Kawamoto S, Yamada I, Azuma M, Takano M, Tokura Y. Magnetocapacitance effect in multiferroic BiMnO$_3$. Phys Rev B 2003;67:180401(R)(4).

[37] Tang J, Feng L, Wiemann JA. Negative magnetoresistance of γ-Fe$_2$O$_3$ observed in γ- Fe$_2$O$_3$/Ag granular nanocomposite. Appl Phys Lett 1999;74:2522–4.

[38] Catalan G. Magnetocapacitance without magnetoelectric coupling. Appl Phys Lett 2006;88:102902(3).

[39] Mukherjee S, Chen CH, Chou CC, Yang HD. Anomalous dielectric behavior in nanoparticle Eu$_2$O$_3$:SiO$_2$ glass composite system. Euro Phys Lett 2010;92:57010(4).

[40] Kao TH, Mukherjee S, Yang HD. Magnetic nanoparticles induced dielectric enhancement in (La,Gd)$_2$O$_5$:SiO$_2$ composite systems. J Magn Magn Mater 2013;346:11–5.

[41] Lukashev P, Sabirianov RF. Flexomagnetic effect in frustrated triangular magnetic structures. Phys Rev B 2010;82:094417(6).

[42] Eliseev EA, Glinchuk MD, Khist V, Skorokhod VV, Blinc R, Morozovska AN. Linear magnetoelectric coupling and ferroelectricity induced by the flexomagnetic effect in ferroic. Phys Rev B 2011;84:174112(16).

[43] Foster AS, Lopez Gejo F, Shluger AL, Nieminen RM. Vacancy and interstitial defects in hafnia. Phys Rev B 2002;65:174117(13).

[44] Nogami M, Moriya Y. Glass formation through hydrolysis of Si(OC$_2$H$_5$)$_4$ with NH$_4$OH and HCl solution. J Non-Cryst Solids 1980;37:191–201.
[45] Rocca F, Ferrari M, Kuzmin A, Daldosso N, Duverger C, Monti F. EXAFS studies of the local structure of Er\(^{3+}\) ions in silica xerogel co-doped with aluminium. J Non-Cryst Solids 2001;293–295:112–7.

[46] Kliava J, Malakhovskii A, Edelman I, Potseluyko A, Petrakovskaja E, Melnikova S, Zarubina T, Petrovskii G, Bruckental Y, Yeshurun Y. Unusual magnetic transitions and nature of magnetic resonance spectra in oxide glasses containing gadolinium. Phys Rev B 2005;71:104406(9).

[47] Kliava J, Malakhovskii A, Edelman I, Potseluyko A, Petrakovskaja E, Melnikova S, Zarubina T, Petrovskii G, Bruckental Y, Yeshurun Y. Reply to “Comment on ‘Unusual magnetic transitions and nature of magnetic resonance spectra in oxide glasses containing gadolinium.’” Phys Rev B 2006;74:026404(2).

[48] Bud’ko SL, Canfield PC. Evaluation of a long-time temperature drift in a commercial quantum design MPMS SQUID magnetometer using Gd\(_2\)O\(_3\) as a standard. J Magn Magn Mater 2006;299:281–7.

[49] Hadjipanayis G, Sellonyer DJ, Brandt B. Rare-earth-rich metallic glasses. I. Magnetic hysteresis. Phys Rev B 1981;23:3349–54.