Abstract
In this paper, we have studied numerically thermo-convective characteristics between a heat transfer fluid (HTF) and phase change material (PCM) in shell and tube thermal energy storage (TES) unit. The paraffin wax is considered as a PCM, filled in a shell which is thermally isolated with the external environment, while the water plays a role of a HTF and flows inside the tube at the moment of charging and discharging cycle. The heat transfer between HTF and PCM is performed by conduction and forced convection, this transfer allows to change the physical state of PCM solid-liquid to obtain a quantity of storable heat in order to create a thermal battery. Enthalpy formulation is used to analyze the heat transfer during melting and solidification process. A good agreement was found between our numerical predictions and the results of the literature. On the other hand, we have investigated the effect of geometrical parameters (tube length and shell diameter) and Reynolds number on the charging and discharging cycles. The obtained results reveal that the tube length and the shell diameter are the most influential parameters on the time of storage system. Similarly, the Reynolds number has much impact on the HTF outlet temperature and the time of solidification and melting process. Furthermore, we have proposed a new thermal storage unit containing the Paraffin wax and RT60 that it gives us a good rate and time of storage compared to the first unit that has only the paraffin wax.

Keywords
heat transfer fluid, phase change material, latent heat storage, shell and tube

1 Introduction
The problems of energies consumption have aggravated due to the increase of industrial, commercial and residential activities; parallely, the current technological development suffers from the depletion of fossil energy. In such case, there is a huge need to use renewable energy sources because they represent a good solution to such problems, and among the known renewable energies, the thermal solar remains the most exploited type. As it is unstable along the time (day and night) and due to its periodic nature, we must use a thermal energy storage device in order to ensure the continuity of this energy during the time. Amongst the types of thermal storage systems, there is the thermal latent heat storage based on the use of phase change materials (PCMs) which have advantages such as high storage density. Many numerical and experimental studies were performed on the latent thermal energy storage systems.

From the previous studies of Yang et al. [1] and Trp et al. [2], the thermal storage depends mainly on the HTF inlet velocity (or mass flow rate), HTF inlet temperature, and geometric parameters. Therefore, the choice of the operating conditions and geometric parameters depends on the required heat transfer rate and the time storage in which the energy will be stored or delivered according to Trp et al. [2]. In order to explore the effect of the adequate choice of the PCM, El Qarnia [3] has studied numerically the thermal performance of a solar latent heat storage unit (LHSU) during charging and discharging cycle by using three kinds of PCMs (n-octadecane, Paraffin wax and Stearic acid) as storage mediums. The results showed that a water production at high temperature depends on the careful selection of PCMs. Recently, Tao and Carey [4] have investigated experimentally the effect of PCM thermo-physical characteristics on the performance of shell and tube LHSU in order to improve its performance. The results have showed that the PCM thermo-physical characteristics are the responsible parameters to improve the time and heat transfer of the system. A phase change process dominated by heat conduction in a shell and tube TES unit has been studied experimentally and numerically by solving a developed analytical model by Kibria et al. [5] for a medium temperature of melting. In order to evaluate the time
of solidification and melting process in terms of HTF outlet temperature, various physical and geometric parameters have been conducted. The results revealed that the inlet temperature of HTF and inner diameter of tube have a strong effect on the heat exchange rate during phase change process compared to the impact of HTF mass flow rate and tube thickness.

A numerical and experimental investigation has been carried out by Hosseini et al. [6] using the commercial paraffin RT50 (Rubitherm GmbH) as PCM. Their results revealed that a rising of HTF inlet temperature from 70°C to 75 and 80°C at a constant flow rate of 1 L/min allows to increase the theoretical efficiency in charging and discharging process from 81.1% to 88.4% and 79.7% to 81.4% respectively. Recently, an experimental study on the vertical shell and tube latent heat thermal storage (LHTS) unit has been conducted by Tao et al. [11] and number of fins, which have a strong effect on the melting the effect of fin thickness is small compared to the fin length influence on the thermal behavior of melting process, whereas results have shown that these parameters have a significant geometric parameters were considered, as the considered shell and tube thermal processes. In order to enhance the heat transfer exchange during such processes, extended surface (fins) are used. As the problem under examination is axisymmetric, the thickness of the inner tube wall is considered; (ii) The thermo-physical properties of HTF and PCM are constant with respect to the temperature; (iii) The initial temperature of the latent thermal storage unit is uniform; (iv) HTF flow is laminar; (v) Natural convection inside the Paraffin wax was not considered, as the considered shell and tube thermal energy storage unit used is horizontal.

During the charging cycle, the HTF flows inside the tube by inlet temperature of 88°C and a mass flow rate of 0.072 kg/min. On the other hand, during the discharging after storage, we took the heat stored using cold HTF passage by a temperature
of 25°C and a mass flow rate of 0.07 kg/min as used in the experimental work of Kibria et al. [5]. The thermo-physical properties of phase change materials with water as HTF which are used in the present investigation are shown in Table 1. This two-dimensional problem is governed by unsteady energy and Navier-stokes equations:

The continuity:
\[
\frac{\partial}{\partial t}(\rho u_i) = 0
\]

The momentum:
\[
\frac{\partial}{\partial t}(\rho u_i) + \frac{\partial}{\partial x_j}(\rho u_i u_j) = \rho \frac{\partial^2 u_i}{\partial x_j \partial x_j} - \frac{\partial p}{\partial x_i} + S_i
\]

The energy:
\[
\frac{\partial}{\partial t}(\rho h) + \frac{\partial}{\partial x_j}(\rho u_i h) = \frac{\partial}{\partial x_i}\left(k \frac{\partial T}{\partial x_i}\right) + S_h
\]

Where \( \rho \) is the density, \( k \) denotes the thermal conductivity, \( \mu \) is the dynamic viscosity, \( S_i \) and \( S_h \) are the source terms, \( u_i \) is the velocity component in the i-direction, \( x_i \) is a cartesian coordinate and \( h \) is the specific enthalpy.

The sensible enthalpy \( h_s \) is given by:
\[
h_s = h_{ref} + \int_{T_{ref}}^T C_p dT
\]

And the total enthalpy, \( H \) is defined as
\[
H = h_s + \Delta H
\]

Where \( \Delta H = \gamma L \) is the enthalpy change due to phase change, \( h_{ref} \) is the reference enthalpy at the reference temperature \( T_{ref} \), \( C_p \) is the specific heat, \( L \) is the specific enthalpy of melting (liquid state) and \( \gamma \) is the liquid fraction during the phase change which occur over a range of temperatures \( T_{solidus} < T < T_{liquidus} \) defined by the following relation 6.(a,b,c):

![Fig. 1 Latent heat storage unit](image)

| Table 1 | Thermo-physical properties of PCMs and HTF [12-14] |
|---------|-----------------------------------------------|
| PCM     | Density [kg/m³] | Specific heat [J/kg K] | Latent heat [J/kg] | Thermal conductivity [W/m K] | Dynamic viscosity [N s/m²] or [kg/m s] | Melting Temperature [°C] |
|         | Solid | Liquid | Solid | Liquid | Solid | Liquid | Solid | Liquid |
| Paraffin wax | 910   | 790    | 2000  | 2150   | 190000 |        | 0.24  | 0.22   | 0.004108 | 61 |
| RT60    | 880   | 770    | 2660  | 2340   | 123506 |        | 0.2   | 0.2    | 0.00003705 | 53–61 |
| Heat transfer fluid (HTF) |        |        |        |        |        |        |        |        |
| Water at 25°C | 997   | 4179   |       |        | 0.613  | 0.000855 |        |        |
| Water at 88°C | 967.1 | 4203   | 0.674 |        | 0.000324 |        |        |        |
If:
\[
\begin{align*}
T < T_{\text{solid\_state}} \quad \text{(solid state)} & : \quad \gamma = \frac{\Delta H}{L} = 0 (a) \\
T_{\text{solid\_state}} < T < T_{\text{liquid\_state}} \quad \text{(Mushy state)} & : \quad 0 < \gamma = \frac{\Delta H}{L} < 1 (b) \\
T > T_{\text{liquid\_state}} \quad \text{(liquid state)} & : \quad \gamma = \frac{\Delta H}{L} = 1 (c)
\end{align*}
\]

3 The Numerical method and the grid used

The governing equations are solved by using the commercial code FLUENT 17 with the first order implicit scheme for the time and the second order upwind scheme for the space. Moreover, the SIMPLE algorithm is used.

The local criterion for numerical convergence, i.e. the maximum relative difference between two consecutive iterations is imposed less than $10^{-6}$. The computational grids in the (xy) plane have been obtained using the non-uniform Quadratic elements type of mesh to simulate the axisymmetric geometry. These structured quadratic cells are created with fine mesh near the walls using mesh generation software ANSYS GAMBIT 2.4.6.

A dense grid distribution is employed near the wall while a uniform grid distribution is used in the streamwise direction. The plots of Fig. 2.a and Fig. 2.b show the typical grid distribution over the computational domain of the configurations I and II. The accuracy of the solution depends on the number and the size of the cells. The grid size used in the computations is chosen by performing a grid independence study (see Fig. 3).

![Fig. 2 The grid used in first (I) and second (II) configuration](image)

For the first configuration, several meshes were tested to ensure that the solution was independent of the mesh (35x300; 50x300; 65x300). This test indicated that 35×300 cells are adequate. On the other hand, concerning the second configuration (Case A and B) the analysis of the grid independency made for the grid tests (50x300; 65x300; 85x300) indicate (not shown here) that 65×300 cells are adequate. From above we can say that the grid (35x300) is suitable for the first configuration and the grid (65x300) is convenient for the second configuration.

4 Results and discussion

Before performing the study of parameters effect on the thermal storage, the validation of the numerical results was performed in charging and discharging cycle through a comparison with the experimental and numerical results of Kibria et al. [5] for the parameters presented in Table 2.

| Table 2 Geometric parameters of the configuration I (configuration of Kibria et al. [5]) |
|---------------------------------------------------------------|
| The inner radius of tube 1 \ ($R_{in1}$) \ [m]                        | 0.0054  |
| The outer radius of tube 1 \ ($R_{out1}$) \ [m]                      | 0.006   |
| The radius of the shell \ ($R_s$) \ [m]                             | 0.018   |
| The length of tube \ ($L_t$) \ [m]                                  | 1       |
| Thickness of tube 1 \ [m]                                          | 0.0006  |

4.1 Validation

The validation was performed on the evolution of HTF outlet temperature at the charging and discharging cycle. The comparison between our numerical results in relation to the analytical and experimental results of Kibria et al. [5] showed a good agreement in Fig. 4.

At the charging cycle, the PCM is initially at solid state (at the temperature 61°C) and the HTF circulates with inlet temperature equal to 88°C, following the boundary and initial conditions of Kibria et al. [5]. The HTF outlet temperature increases over time until asymptotic value of 83°C which is lower than the inlet temperature (88°C). This difference is due to the heat absorption by melting Paraffin wax. The results show
that the outlet temperature of system is close to those obtained analytically and experimentally by Kibria et al. [5], where this process took about 6500s to complete the charging cycle. In discharging process, the HTF absorbs the heat stored in the Paraffin wax whereas the HTF outlet temperature decreases over time until asymptotic value 33°C and the paraffin wax becomes in the solid state. The small discrepancy between the numerical results and those obtained experimentally is due to the simplifications considered in the numerical model. Further validations (not shown here) done for several parameters give a good agreement with the numerical and experimental data of the literature [5].

4.2 Parametric study

In this investigation, we have made a parametric study following the measures of the first configuration (Table 2) based to examine the effect of: (i) length of tube; (ii) shell diameter; and (iii) Reynolds number on the time and rate of charging and discharging process. Furthermore, we have tried to propose a new thermal unit composed of a Paraffin wax and RT60. The performances of this new configuration will be compared to the first one.

4.2.1 Influence of tube length

Fig. 5 shows the effect of different tube length $L_t$ on the thermal performance during the charging and the discharging cycles. Considering the first configuration, we have changed the tube length in the range 0.2-1.8m in the scope to quantify this effect for the charging and discharging cycles. From this figure which depicts outlet temperature of HTF versus the tube length variation in the range 0.2-1.8m. We can see that the time of charging and discharging cycles is proportional to the tube length. An increase of the length leads to an increase of the melting and solidification time. Moreover, the increase of tube length decreases the asymptotic value of the HTF outlet temperature from 87°C in the case $L_t=0.2$m to 79°C in the case $L_t=1.8$m during 5600s. This leads to a gradient of temperature $\Delta T_{ch}$ equal to 8°C between HTF outlet temperatures of tube
length from 0.2m to 1.8m at charging time. With regard to the discharging process and the effect of increasing the tube length, the asymptotic value of the HTF outlet temperature increases from 25°C to 38.5°C along the 5600s, thus leading to a gradient of temperature $\Delta T_{\text{dis}}$ equal to 13.5°C. From this figure, it can be seen that the tube length is an important parameter to optimize the melting and solidification time.

### 4.2.2 Effect of shell diameter

The shell diameter is among the important parameters that have a relation with the progress of solidification and melting. In this case we have changed the shell diameter in the range 24-44 mm. Fig. 6 shows that the shell diameter reduction allows to complete the discharging and charging rate in a short time. The reduction of shell diameter causes the minimizing of the PCM mass volume. This allows accelerating the heat charging or discharging of the mass through heat transfer process. This contributes to speed up the melting fraction rate of the Paraffin wax during charging process.

It can be seen from the figure, that the shell diameter of 24 mm needs just 3300s to complete almost the charging or the discharging processes, whereas the other cases needed more than 5000s to complete the fully charging or discharging processes. As a result, the gradient in HTF outlet temperature between the shells of minimum and maximum diameter used $\Delta T_{\text{ch}}$ is equal to 5°C for charging process and $\Delta T_{\text{dis}}$ is about 8°C for discharging process. Therefore, the quantity of Paraffin wax must be appropriate with the work conditions, in order to optimize the time of storage system.

### 4.2.3 Effect of Reynolds number

As we know, the Reynolds number depends on the HTF properties as the viscosity, velocity, and the size of the tube. In the present investigation, only the laminar regime is considered for the flow of HTF. In this contribution, the effect of Reynolds number is investigated in the range Re= 100-1500. The increase of Reynolds number allows to decrease the solidification and melting time as shown in the Fig. 7. It is clear from this figure, that for the charging cycle and for the high value of Reynolds number (Re=1500) the HTF outlet temperature tends to reach the asymptotic value of 86.5 °C, while for the lower value of Reynolds number (100), the HTF outlet temperature tends to reach the asymptotic value of 69.5°C. Therefore, the temperature gradient $\Delta T_{\text{ch}}$ of HTF outlet temperature in discharging cycle is about 9.6°C and in the charging case $\Delta T_{\text{ch}}$ is 17°C.

### 4.2.4 Improvement of TES unit

According to the above results, it could be very useful to find an effective way that allows the PCM to absorb the maximum heat provided by the HTF. As a result, we have tried to propose a new configuration (Fig. 1(d)), where we inserted a layer of another phase change material namely the RT60, that its melting temperature is equal to 57 °C, which is very close to melting temperature of the paraffin wax (equal to 61 °C). This layer of RT60 makes it possible to distribute the thermal load on the paraffin wax along the axial direction and to ensure it the thermal inertia. In this TES unit, the two PCMs are superposed between the copper tubes. Therefore, the heat exchange in this unit is done by conduction in two steps; (i) heat interchange between HTF and RT60 through the first copper tube, (ii) heat transfer from the RT60 into the paraffin wax through the second copper tube. The same boundary and initial conditions adopted in the first configuration are used here. Different cases according to Table 3 and Table 4 are numerically predicted. The melting temperature of RT60 is lower than the paraffin wax (61°C), which allows the RT60 to melt before the paraffin wax, which leads to accelerate the melting process of RT60 and its solidification process due to its rapid heat absorption from the HTF.

In this configuration we proposed two cases A and B. The case A (see Table 3) has a constant radius of the shell $R_{\text{sh}}$ and a variable inner radius of the second tube $R_{\text{in2}}$ that consequently reduces the volume of Paraffin wax. This radius is varied in the
range 0.008-0.014m. The variation of the inner radius allows us to obtain several proportions in the volume of the two PCMs, from the case the existence of only the Paraffin wax to the case we obtain the Paraffin wax with RT60 ($R_{in2}=0.014m$). The results shown in Fig. 8 indicate a decrease in the time of charging and discharging cycles compared to case of the first thermal storage unit (containing only Paraffin wax), whereas the temperature gradient $\Delta T_{ch}$ of the HTF outlet temperature in charging cycle increases in the first time period [0-1500s], then starts to decline. Near the time 4000s, we remark an increase of the outlet temperature and $\Delta T_{ch}$. This is due to the PCMs which have achieved the total phase change from the solid to liquid and we are in sensible phase of heat transfer. In case B (Table 4), we have fixed the volume of Paraffin wax (same volume of the first configuration) and we have varied the inner radius of the second tube $R_{in2}$ from 0.008 to 0.014m, which means the shell radius will vary. In this case the time of charging and discharging cycle also decreases compared to the use of a Paraffin wax alone as presented in Fig. 9. This case is more stable in charging and discharging cycles than case A, as the mass volume of the PCMs of the case B is increased compared to the first case A. However, both cases have a better evolution of the HTF temperature than the paraffin wax alone as shown in Fig. 8 and Fig. 9.

5 Conclusion
As the appropriate choice of the physical and geometric parameters allows to optimize the thermal storage unit, the present study was devoted to examine the effect of these parameters on the shell and tube thermal energy storage unit that investigated previously by Kibria et al. [5]. Moreover, improvements of this storage unit were investigated through new configurations. A two-dimensional numerical method based on the Enthalpy formulation has been used to predict the heat transfer between HTF and PCM. The laminar forced convection inside the tube during charging and discharging process was considered, whereas the natural convection has been ignored inside the PCM enclosure.

| Table 3 Geometric parameters of the second configuration II.A |
|---------------------------------------------------------------|
| The inner radius of tube 1 ($R_{in}$) [m] 0.0054              |
| The outer radius of tube 1 ($R_{ou1}$) [m] 0.006              |
| The inner radius of tube 2 ($R_{in2}$) [m] 0.008 0.01 0.012 0.014 |
| The radius of the shell ($R_{sh}$) [m] 0.018                  |
| The length of tube ($L_t$) [m] 1                             |
| The thickness of copper tube 1 and 2 [m] 0.0006               |

| Table 4 Geometric parameters of the second configuration II.B |
|---------------------------------------------------------------|
| The inner radius of tube 1 ($R_{in}$) [m] 0.0054              |
| The outer radius of tube 1 ($R_{ou1}$) [m] 0.006              |
| The inner radius of tube 2 ($R_{in2}$) [m] 0.008 0.01 0.012 0.014 |
| The radius of the shell ($R_{sh}$) [m] 0.01902 0.02001 0.02114 0.02239 |
| The length of tube ($L_t$) [m] 1                             |
A parametric study has been conducted in order to study the effect of the tube length, shell diameter and Reynolds number. Improvement of the thermal performances of this unit was proposed and investigated.

The results of the parametric study have shown that the tube length and shell diameter have a great effect on the HTF outlet temperature, moreover the Reynolds number is the most influential parameter which has an impact on the time and rate of solidification and melting process.

From the present results, the design parameters should be selected carefully in order to optimize the performance of the storage unit. In addition to that, the new thermal energy storage unit filled by RT60 and Paraffin wax allowed for better efficiency of rate storage and HTF outlet temperature compared to the unit containing only the Paraffin wax.

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