The incidence of magnetic fields in cool DZ white dwarfs

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Accepted 2015 March 12.

ABSTRACT

Little is known about the incidence of magnetic fields among the coolest white dwarfs. Their spectra usually do not exhibit any absorption lines as the bound-bound opacities of hydrogen and helium are vanishingly small. Probing these stars for the presence of magnetic fields is therefore extremely challenging. However, external pollution of a cool white dwarf by, e.g., planetary debris, leads to the appearance of metal lines in its spectral energy distribution. These lines provide a unique tool to identify and measure magnetism in the coolest and oldest white dwarfs in the Galaxy.

We report the identification of 7 strongly metal polluted, cool ($T_{\text{eff}} < 8000$ K) white dwarfs with magnetic field strengths ranging from 1.9 to 9.6 MG. An analysis of our larger magnitude-limited sample of cool DZ yields a lower limit on the magnetic incidence of $13 \pm 4$ percent, noticeably much higher than among hot DA white dwarfs.

Key words: stars: white dwarfs - stars: magnetic field - stars: planetary systems - stars: evolution

1 INTRODUCTION

White dwarfs (WDs) have been known to harbour magnetic fields since the detection of circularly polarised light from GJ 742 (Kemp et al. 1970). In the following decades a plethora of magnetic WDs (MWDs) have been identified either from Zeeman splitting of absorption lines in their spectra or by spectropolarimetry (Kawka et al. 2007, and references therein). A wide variety is seen in temperature, atmospheric composition, and field strength. The advent of large scale spectroscopic surveys, in particular the Sloan Digital Sky Survey (SDSS), has in the last decade increased the number of known MWDs to several hundred (G"ansicke et al. 2002; Schmidt et al. 2003; Vanlandingham et al. 2005; Kleinman et al. 2013; Kepler et al. 2012, 2013).

Despite the ever growing list of these previously rare objects, two questions continue to remain without a definite answer: What is the origin of these magnetic fields? And what is the fraction of WDs that are magnetic, and how does this vary with cooling age/temperature?

Two distinct models have been proposed to explain the emergence of fields $\gtrsim 1$ MG in isolated WDs. In the fossil field hypothesis, the magnetic fields of the chemically peculiar Ap/Bp stars are thought to be amplified due to flux conservation during post-main sequence evolution, resulting in WDs with fields in the MG regime (Woltjer 1964; Angel & Landstreet 1975; Angel et al. 1984; Wickramasinghe & Ferrario 2000). A more recent hypothesis (Tout et al. 2008) considers a binary origin, where a system undergoing a common envelope leads to magnetic dynamo generation.

The incidence of magnetism in WDs remains poorly estimated due to selection effects. Independent studies are difficult to reconcile with one another as each suffers from its own set of biases. This problem becomes significantly more pronounced when focusing on subsets of the total WD population where small number statistics dominate. Recent volume limited samples of nearby WDs present the most unbiased estimates of the magnetic incidence when considering all WD sub types, and suggest incidences of $21 \pm 8$ percent for WDs within 13 pc of the Sun, and $13 \pm 4$ percent for those within 20 pc (Kawka et al. 2007). However these MWDs are dominated by fields lower than 100 kG and strongly magnetic objects with fields above 10 MG. Only 1 out of the 15 MWDs in the compilation of Kawka et al. (2007) has a field strength between 1 and 10 MG (the range that we discuss in this work). More recently, Sion et al. (2014) have presented a volume limited WD sample within 25 pc from the Sun. They find a magnetic incidence of 8 percent when considering magnetic fields above 2 MG only. Other studies have investigated the magnetic incidence with much larger, but magnitude-limited samples. For instance Kleinman et al. (2013) identified over 12000 DA\textsuperscript{1} from SDSS data release 7

\textsuperscript{1} WDs showing only hydrogen/helium lines in their spectra are classified DA/DB, with only metal lines as DZ, and without any spectral lines as DC. Magnetic DA WDs where magnetism is de-
(DR7) spectra, of which over 500 are suggested to be magnetic (Kepler et al. 2013), leading to a much lower incidence of 4 percent. However, because this sample is magnitude-limited, it is intrinsically biased. Most degenerates in the local sample have temperatures below 10000 K, whereas 84 percent of the WDs from Kepler et al. (2013) are hotter than this. The discrepant numbers between the local sample of cool/old WDs and hotter/younger WDs, have been the basis for some authors to claim an age-dependency of the magnetic incidence (Fabrika & Valyavin 1993; Liebert et al. 2003).

Analysing the small sample of WDs with accurate parallaxes, Liebert (1988) noted that magnetic WDs appear to be under-luminous for their colour, suggesting they have smaller radii, and hence higher masses, than non-magnetic WDs. Later, Liebert et al. (2003) derived a mean mass of 0.93 $M_\odot$ for eight MWDs from the Palomar Green (PG) survey, based on model atmosphere analyses, compared to ~0.6 $M_\odot$ for non-magnetic ones. While there is hence independent evidence for higher-than-average masses for MWDs, caveats to bear in mind are that there are still few MWDs with precise parallaxes, and even for those systematic uncertainties in the analysis of their spectra limits the accuracy of the desired masses (Külebi et al. 2010).

A common theme among all the above investigations is that the true magnetic incidence is expected be higher, as the various biases (e.g. signal-to-noise, magnetic broadening) tend to work against the identification of MWDs.

The very coolest WDs ($T_{\text{eff}} < 8000$ K) do not show optical lines of hydrogen or helium since these elements are in their ground states in the low temperature atmospheres. This transition to featureless (DC) spectra occurs at around 11000 K for WDs with helium dominated atmospheres, and 6000 K for WDs with hydrogen dominated atmospheres (Vauclair et al. 1981; Bergeron et al. 2001). Because of this absence of absorption lines, it is not possible to identify magnetism in these stars via Zeeman splitting. A handful of DCs have been found to be magnetic through spectropolarimetry (Putney 1997). However, this method is expensive and is unsuitable for most known cool WDs because of their faintness.

## 2 METAL POLLUTED WHITE DWARFS

The last two decades have seen great interest devoted to the study of WDs with atmospheres contaminated by metals. The now widely accepted scenario is that after post-main sequence evolution to the WD stage, an accompanying planetary system will undergo dynamical instability (Debes & Sigurdsson 2002; Veras et al. 2013). Small rocky bodies such as asteroids or minor-planets may then have their orbits perturbed by a larger planetary object and soon find themselves venturing into the Roche-radius of the WD, resulting in their tidal disruption (Debes et al. 2012; Veras et al. 2014) and subsequent formation of a circumstellar debris disk. This material is then accreted onto the star (Jura 2003; Rafikov 2011) producing metal lines in the spectra of these WDs.

Cool WDs displaying only metal lines are classified as DZ. Farihi et al. (2010) showed that DZ and DC white dwarfs share the same velocity, spatial and temperature distributions and should therefore belong to the same stellar population. Assuming the existence of magnetism among DZ stars is uncorrelated with the presence of metals, the detection of split metal lines in the spectra of DZ white dwarfs becomes a powerful tool for determining the magnetic field strength distribution among the very coolest and oldest of WDs. However, prior to this work, only 3 magnetic DZ WDs were known: LHS2534 (Reid et al. 2001), WD0155+003 (Schmidt et al. 2003), and G165-7 (Dufour et al. 2002), with respective surface averaged field strengths, $B_s$, of 1.9, 3.5, and 0.6 MG. These all have SDSS spectra and so we refer to these using the SDSShmm±ddmm naming format (SDSS1214−0234, SDSS0157+0033, and SDSS1330+3029 respectively) for consistency with our new identifications and the names used in Koester et al. (2011).

Recently, Koester et al. (2011) identified a sample of 26 cool ($T_{\text{eff}} < 9000$ K) DZ with strong photospheric metal pollution, filling previously empty parameter space at low $T_{\text{eff}}$ and high atmospheric Ca abundance compared with the preceding work by Dufour et al. (2007). The rocky nature of the accreted material is evident from the variety of detected metals which includes Ca, Mg, Fe, Na, Cr, and Ti, and the low abundance of H. The Koester et al. (2011) sample also includes re-identifications of the known magnetics SDSS0157+0033 and SDSS1330+3029 (see above).

## 3 RESULTS

### 3.1 Identification

In an extension of the work by Koester et al. (2011) using the more recent DR10 spectroscopic data, we have identified a sample of 79 strongly polluted cool DZ, with the serendipitous discovery that 10 are magnetic. Full details of this sample will be presented elsewhere (Hollands et al. in prep); here we only provide a brief summary of the selection procedure.

Firstly, we queried SDSS Casjobs (Li & Thakar 2008) for objects with colours below the main sequence in the $(u-g)$ vs. $(g-r)$ two-colour diagram (Figure 1). This region of colour-space is highly abundant in quasars of redshift 2–5. To remove these, we employed two independent cuts in proper-motion and redshift: a minimum proper-motion threshold of 3-$\sigma$ above zero and SDSS spectroscopic redshift below 0.01. Any spectrum with non-zero redshift ZWARNING (0 indicates no warning) was also kept.

Requiring the objects to pass at least one of the proper-motion or redshift selection criteria was necessary as neither could be completely relied upon in isolation. On the one hand, proper motions may be unavailable if the object is too faint to be detected in the USNO-B images used to detect positional variations. Additionally, because detectable cool DZ are by definition relatively nearby (as they are intrinsically faint), some will have sufficiently high proper-motions to evade a match between SDSS and USNO-B observations. On the other hand, the unusual spectra of DZ WDs with their deep, broad metal lines can trick the SDSS redshift pipeline into classifying them as quasars, reporting values of $z > 1$, with ZWARNING = 0.
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Figure 2. Optical SDSS spectra for all 10 magnetic DZ, ordered from top to bottom by increasing magnetic field strength. Data are smoothed by a 7-point boxcar to reduce the noise level and enhance spectral features, with the exception of the bright object SDSS1330+3029. Insets are plotted where splitting is not obvious in the full spectrum (same smoothing applied).
Ca triplet), we are able to identify split lines of either Mg i, Na i, or both. For field strengths of \( \gtrsim 2 \) MG, spin and orbit angular momenta decouple, and so the Paschen-Back approximation is appropriate. Therefore we treat the splittings as triplets.

We used a 7-parameter fit to the observed line profiles to measure the field strength. The continuum flux in the vicinity of the triplet was modelled as a quadratic in \( F_\nu \). A linear approximation would not suffice, particularly for the wings of the broad Mg feature (see Figure 2). We then modelled the triplet as the sum of three Gaussian profiles with equal width, depth (in continuum normalised flux) and separation in wavenumber, \( \lambda/\nu \). The wavenumber of the \( \pi \)-component of the triplet was also included as a free parameter to account for small shifts. In all cases, we found the \( \pi \)-components are blue shifted from their rest wavelengths, and generally increasing with field strength, suggesting this is predominantly caused by the quadratic Zeeman effect, with only minor contributions from gravitational and Doppler shifts. The maximum blueshift of the \( \pi \)-component is found to be 5 Å for the Na triplet of SDSS1536+4205. The small (few percent) measurement error this may have on our field measurements does not affect our discussion on magnetic incidence.

We used least-squares minimisation via the Levenberg-Marquardt algorithm to optimise these parameters. Where possible we fitted both the Mg and Na lines, however, this could not always be achieved for a variety of reasons: One of the lines may be significantly less deep than the other; the Mg line in some cases is very broad and asymmetric, such that the 3 components cannot be distinguished; or poor subtraction of sky emission distorts the flux near the \( \pi \) component of the Na triplet, making a fit to this line less reliable than for the Mg triplet.

The average surface magnetic field strength, \( B_S \), was subsequently calculated from

\[
\frac{B_S}{\text{MG}} = \frac{\Delta(1/\lambda)}{46.868},
\]

where \( \Delta(1/\lambda) \) is the inverse wavelength separation in cm\(^{-1} \) between the components of a triplet \( \pi \)-component is found greater than for the Mg triplet.

3.2 Average magnetic field measurement and effective temperatures

In the spectra of all 10 objects (with the exception of SDSS1330+3029 where Zeeman splitting is only seen in the
Magnetic DZ with field strengths, temperatures and SDSS PSF photometry. Previously known magnetic DZ are indicated by their starred coordinates. The field strengths for SDSS1214−0234 and SDSS1330+3029 are taken from Reid et al. (2003) and Dafour et al. (2006) respectively. The quoted $B_S$ uncertainties are obtained from the formal errors on our fit parameters. Where a good fit is obtained for both Mg and Na lines, their weighted mean is used.

| SDSS          | $B_S$ (MG) | $T_{\text{eff}}$ (K) | $u$ (mag) | $g$ (mag) | $r$ (mag) | $i$ (mag) | $z$ (mag) |
|---------------|------------|----------------------|-----------|-----------|-----------|-----------|-----------|
| J133059.26+302953.2* | 0.65       | 6000                 | 18.28 ± 0.02 | 16.32 ± 0.02 | 15.89 ± 0.01 | 15.91 ± 0.02 | 16.09 ± 0.03 |
| J090222.98+362539.6  | 1.92 ± 0.05 | 6300                 | 22.58 ± 0.32 | 20.75 ± 0.03 | 20.46 ± 0.04 | 20.36 ± 0.06 | 20.50 ± 0.22 |
| J121456.39−023402.7* | 1.92       | 5200                 | 20.87 ± 0.06 | 18.32 ± 0.02 | 17.75 ± 0.01 | 17.58 ± 0.01 | 17.51 ± 0.02 |
| J085320.38+410937.9  | 2.35 ± 0.11 | 5900                 | 23.62 ± 0.79 | 21.32 ± 0.05 | 20.63 ± 0.03 | 20.70 ± 0.05 | 20.75 ± 0.14 |
| J115224.51+160546.7  | 2.72 ± 0.04 | 6500                 | 21.73 ± 0.12 | 20.18 ± 0.03 | 19.95 ± 0.02 | 20.02 ± 0.03 | 20.08 ± 0.09 |
| J015748.14−003315.0* | 3.49 ± 0.05 | 5700                 | 21.30 ± 0.07 | 19.59 ± 0.02 | 19.19 ± 0.02 | 19.21 ± 0.02 | 19.36 ± 0.05 |
| J100346.66−003123.1  | 4.37 ± 0.05 | 6300                 | 22.91 ± 0.33 | 20.61 ± 0.03 | 20.06 ± 0.02 | 20.00 ± 0.03 | 20.20 ± 0.11 |
| J073549.19+205720.9  | 6.12 ± 0.06 | 6000                 | 23.08 ± 0.34 | 20.53 ± 0.02 | 19.98 ± 0.02 | 19.92 ± 0.02 | 20.09 ± 0.09 |
| J232538.93+044813.1  | 6.56 ± 0.09 | 7200                 | 21.44 ± 0.15 | 19.88 ± 0.02 | 19.58 ± 0.03 | 19.68 ± 0.04 | 19.69 ± 0.11 |
| J153642.53+420519.2  | 9.59 ± 0.04 | 5500                 | 23.32 ± 0.65 | 20.84 ± 0.04 | 20.30 ± 0.03 | 20.17 ± 0.04 | 20.33 ± 0.16 |

Figure 3. Fits to the Mg and Na splittings for SDSS1536+4205. Lines are fit with Gaussians with equal $1/\lambda$ separations from the central $\pi$ components.

3 Served from any inclination to the magnetic axis can not reproduce these line profiles.

This suggests that these WDs may have more complex field topologies. We show that a dipole offset from the star’s centre can reproduce the observed Zeeman line profiles. In principle this offset, $a$, can be in any direction relative to the unshifted magnetic field axis (Achilleos & Wickramasinghe 1988), however, here we consider only displacement along the magnetic dipole axis (which we define to be in the $z$-direction), i.e. $a_z = a_0 = 0$ as in Achilleos et al. (1992).

For an arbitrary point on the surface of the WD with coordinates $(x, y, z)$ in units of $R_{\text{WD}}$, the strength of the field, $B(x, y, z)$, is given by (Achilleos et al. 1992)

$$B(x, y, z) = B_d \left[ r^2 + 3(z - a_z)^2 \right]^{1/2} / 2r^4,$$

where $a_z$ is the dipole offset, $B_d$ is the dipolar field strength and

$$r^2 = x^2 + y^2 + (z - a_z)^2.$$ These equations can be used to compute synthetic Zeeman line profiles given for a given $B_d$, $a_z$, and line-of-sight inclination to the magnetic axis, $i$. In our model we firstly generate a set of 10000 points randomly distributed over the projected surface of the WD. At each point the magnetic field strength is evaluated using equation (2), accounting for the inclination of the magnetic axis, and the corresponding Zeeman line profiles are generated as a sum of 3 Gaussians separated according to equation (1). These profiles are then coadded with weights proportional to the limb darkening corresponding to the location on the star. We use limb darkening coefficients appropriate for a 6000 K, log $g = 8$ WD from Gianninas et al. (2013), adopting the logarithmic limb darkening law described therein.

We fitted the above model to the Zeeman lines in SDSS1536+4205 using the affine invariant MCMC sampler, emcee. Replacing $B_S$ with $B_d$ and including the inclination and dipole offset, increased the number of free parameters in the fit (compared with 1–11 to 9. Uninformed priors were used for variables with a physically constrained range. E.g.

3 $B_d$ is defined in such a way that the magnetic field has this strength at $z = a_z \pm 1$ WD radii along the magnetic axis.
−1 < a_z < +1 forces solutions with the dipole centre confined within the stellar surface. For the line-of-sight inclination to the magnetic axis, the prior distribution \( P(i) \propto \sin i \) was employed.

Since SDSS1536+4205 shows distinctly split lines of both Mg and Na, both were fitted independently. The values for \( B_d \), \( i \), and \( a_z \) are shown in Table 2 with the resulting best fits to the spectra shown in Figure 3. While the line profiles appear similar to the simple model shown in Figure 3, it should be recalled that we have now fitted a physical model capable of reproducing the observed narrow Zeeman lines rather than the assumption of unbroadened lines used in Section 3.2.

The fit to the Mg triplet has a slightly worse reduced \( \chi^2 \) than to the Na triplet. This is the result of the Mg line having an intrinsically asymmetric profile due to quasi-static broadening of this transition (Wehrse & Liebert 1981; Koester et al. 2011). Therefore assuming a Gaussian profile limits the quality of the fit. Nevertheless, the resulting parameters from the Mg and Na fits are in agreement within their (similarly large) uncertainties.

While the inclination uncertainties permit a wide range of values within the allowed parameter space (0°–90°), the results for \( B_d \) and \( a_z \) strongly suggest an offset dipole. However, it should be noted that \( B_d \) and \( a_z \) are highly anti-correlated, with a correlation coefficient of −0.99 for both fits. The values of \( a_z \) we find are well within the range of those found for SDSS DAWDs (Külebi et al. 2001).

The fit values of \( B_d \), \( i \), and \( a_z \) have the following physical interpretation: An offset dipole leads to a strong field emerging at one of the poles of SDSS1536+4205, (≈ 50 MG according to equation 2), with the opposite hemisphere exhibiting a very uniform field strength of 9.6 MG as in Table 2. The value of inclination and sign of \( a_z \) imply that most of the WD surface with high fields is obscured when viewed from the Earth, with only a small amount of this region entering the limb of the star. Hence the \( \sigma \) components of the Zeeman lines are broadened only slightly with their depths reduced by a few percent.

### Table 2. Results from our MCMC fits to SDSS1536+4205 assuming an offset dipole field structure. Quoted values and uncertainties errors are, respectively, the 50th, 15.9/84.1th percentiles of the posterior probability distributions. Reduced \( \chi^2 \) values are calculated using the median for each parameter.

| Parameter       | Mg   | Na   |
|-----------------|------|------|
| \( B_d \) (MG)  | 18.6±2.2 | 20.0±1.6 |
| inclination (°) | 31±14 | 41±16 |
| \( a_z \) (%RWD) | −23.9±4.3 | −28.8±5.5 |
| reduced \( \chi^2 \) | 1.25 | 0.97 |

4 NOTES ON INDIVIDUAL OBJECTS

**SDSS0157+0033.** The value of \( B_d \) given by Schmidt et al. (2003) is 3.7 MG, whereas we obtain a value of 3.49 ± 0.05 MG using the same SDSS spectrum. Schmidt et al. (2003) arrive at this value from measuring both the Mg and Na lines. For the Na triplet, only two of the Zeeman components can be identified in the noisy spectrum, and their centres are difficult to locate. For the Mg triplet, where all three Zeeman components are well resolved, we have noticed that Schmidt et al. (2003) report a position for the \( \sigma^- \) line (5128 Å) which is about 7 Å bluer than we measure leading to an overestimate of \( B_d \). We therefore suggest 3.49 ± 0.05 MG as a revised value for this star’s surface average magnetic field strength, which we quote in Table 2.

**SDSS0735+2057** exhibits an extremely broad Mg feature, and close examination reveals Zeeman split lines at its base. None of the other 78 DZ in our sample shows an Mg line like this. It seems likely that the unusual Mg profile is a direct result of the magnetic field partially splitting an already broad feature. SDSS2325+0448 has a similar surface-averaged field strength and so one might suspect a similarly broadened Mg triplet, which is not observed. The stark difference between their line profiles can be explained by higher metal abundances and lower \( T_{\text{eff}} \) for SDSS0735+2057. This increased opacity that the magnetic induces in the Mg feature will need to be considered when calculating chemical abundances (Hollands et al. in prep). The formal errors on \( B_d \) (Table 1) are surprisingly small, at the level of ~1 percent, however the values obtained from the Mg and Na lines for this star agree to within 1.3\( \sigma \) (6.24 ± 0.11 MG and 6.08 ± 0.07 MG respectively). We adopt the weighted mean of these as the measured value in Table 1.

**SDSS1536+4205** has the strongest magnetic field of any known DZ, with \( B_d = 9.59 ± 0.04 \) MG. We also obtain very consistent field measurements between the Mg and Na lines, 9.57 ± 0.08 MG and 9.60 ± 0.04 MG respectively, indicating the uncertainties are not underestimated. Again the final value presented in Table 1 is the weighted average of these two independent measurements. The Zeeman split lines of Mg and Na for this WD are well resolved from the noise, yet do not show any significant magnetic broadening, as discussed in detail in (52) and (55). We also note that this
object may show an emission line at approximately 8400 Å. This peculiar feature does not coincide with any sky line, and peaks at 4σ above the continuum. Additionally, the feature is visible in multiple SDSS sub-spectra. Checking spectra from adjacent fibers observed on the same night and plate does not indicate flux contamination from other fibers, and neither does inspection of the SDSS images reveal any nearby bright stars. If this emission is real, the most plausible identification is O I. We note that a few cool DQ WDs show oxygen emission lines (Provencal et al. 2005), the origin of which is still uncertain. A higher S/N spectrum will be required to determine whether this feature in SDSS is genuine.

5 DISCUSSION

5.1 Magnetic incidence

We have amassed a sample of 79 DZ WDs with colours that place them below the main sequence in the (u − g) vs. (g − r) plane. We identify 10 of these to be magnetic (Table 1), leading to an observed incidence of 13 ± 4 percent purely for this sample. Our selection procedure only uses colour, redshift and proper-motions. Since colours will not be significantly altered by the presence of a magnetic field, we believe this selection procedure to be unbiased towards (or against) selection of magnetic objects. This is not to say this sample is free from biases. On the contrary, various selection effects, which we discuss in the following sections, suggest that our measured magnetic incidence is only a lower limit.

We report DZ to be magnetic only where we confidently detect Zeeman splitting. The major limitation in detecting splitting of spectral lines are S/N and spectral resolution.

The vast majority of our 79 DZ have S/N ratios of 5–6. While this is sufficient to identify the pressure broadened absorption features characteristic of cool DZ, detecting fields below 2 MG is not possible. For example, SDSS1152+1605 was identified from a spectrum observed with the SDSS spectrograph (Koester et al. 2011) at a S/N ratio of ~5. Although Koester et al. (2011) speculated that this object may be magnetic, the quality of the data available to them was insufficient for a firm conclusion. Its newer BOSS spectrum clearly reveals Zeeman splitting (S/N ratio of 9). We show a comparison of these two spectra in Figure 5.

Inspecting the cumulative distribution in field strengths (Figure 6) demonstrates the difficulty in detecting magnetism for B S < 2 MG. Above ~1.9 MG, the distribution is approximately linear in log(B S), which is consistent with the distribution seen in other WD samples (Kawka et al. 2007). Below this value the only MWD found is SDSS1330+3029 (B S = 0.65 MG), which is made possible by the exceptional S/N of its spectrum. This suggests that several objects with lower quality spectra may have magnetic fields between 0.65 and 1.9 MG.

As for resolution, the BOSS instrument has a resolving power of approximately 2000 (Smee et al. 2013). This implies a minimum detectable field via Zeeman splitting of a few hundred kG, and so SDSS1330+3029 is representative of the lowest detectable field for DZ in SDSS.

5.2 Magnetic field origin and evolution

While the true incidence of magnetism among WDs on the whole is still widely debated, estimates between 5–10 percent are common for isolated degenerate objects (Wickramasinghe & Ferrario 2000; Liebert et al. 2003; Sion et al. 2014). It has been suggested that older (cooler) WDs exhibit a higher incidence of magnetism (Kawka & Vennes 2014; Liebert et al. 2003), which at face value is supported by the large fraction of cool MWDs in our sample. However, we can at present not exclude that the high incidence of magnetism is linked to the presence of metals in the atmospheres of the cool DZ, e.g. through (merger) interaction with planets.
In addition, the origin of magnetic fields among WDs remains under discussion with the most plausible mechanisms proposed being:

(i) From the intial-to-final mass relation and main sequence lifetime as a function of stellar mass, most of the known WDs are thought to have evolved from A and B type stars. These stars are known to exhibit magnetic fields (Angel et al. 1981; Wickramasinghe & Ferrario 2000; Neiner et al. 2014), with the peculiar Ap and Bp stars having comparatively higher fields. As the star evolves off of the main sequence it is expected that the magnetic flux of the progenitor star is conserved and so the change in stellar radius amplifies the surface field, i.e. \( B_{\text{WD}}/B_{\text{MS}} = (R_{\text{MS}}/R_{\text{WD}})^2 \). This is known as the fossil field hypothesis, and can produce WDs with field strengths in the observed range (Woltjer 1964; Angel & Landstreet 1970; Angel et al. 1981; Wickramasinghe & Ferrario 2000).

Ohmic decay is expected to cause magnetic fields to decrease in strength with time. However, the timescale for this is expected to be of the order \( 10^{10} \) yr due to the high electrical conductivity in the degenerate cores of WDs (Wendell et al. 1982). Therefore the fossil field hypothesis is not unreasonable for describing the field origin in the old WDs we identify in this work.

However, recent estimates of magnetic incidence exceeding 10 percent (Liebert et al. 2003; Kawka et al. 2007; Sion et al. 2014), challenge the fossil field hypothesis. The space density of Ap/Bp stars is insufficient to account for all the known MWDs with \( B_S > 1 \) MG (Kawka & Vennes 2004), and so at least one other evolution channel is required for producing MWDs.

(ii) Tout et al. (2008) suggested that WDs with \( B_S > 1 \) MG are the products of an initial binary origin. Stellar evolution of one of the binary components can lead to a common envelope (CE) stage. It is during this phase that a magnetic dynamo may be generated within the CE. The resulting field then persists beyond the lifetime of the CE, within the now close binary or merged single object. For a close binary, a merger may take place later.

The binary origin of these highly magnetised WDs naturally leads to higher masses than the canonical 0.6 M\(_\odot\) for non-magnetic WDs, compatible with the observation that MWDs are typically more massive than non-magnetics (Liebert 1988; Liebert et al. 2003).

However, a binary origin would in our case raise questions about how these WDs come to be polluted by material from a remnant planetary system. This model need not be constrained only to stellar binaries. Nordhaus et al. (2011) suggested that the engulfment of gaseous planets or brown dwarf companions during the asymptotic giant branch (AGB) phase could also lead to magnetic dynamo generation and eventually a high field nwd, in this scenario, mwdw would not be expected to have higher masses than non-magnetics, but it would allow for evolved planetary systems which later pollute the wd with metals. Farihi et al. (2011) identified a cool (\( T_{\text{eff}} = 5310 \) kK) magnetic (\( B \approx 120 \) kG) DAZ white dwarf, and speculate on that basis that the WD underwent a CE with a closely orbiting gas giant planet during the progenitor star’s AGB phase, leading to the emergence of a magnetic field. If this is indeed the mechanism from which magnetic fields are produced in DZ, it may explain the particularly high magnetic incidence found in our sample.

Unlike the fossil field hypothesis, the giant planet CE scenario would be correlated with the presence of metals in the atmospheres of WDs, where the metal lines are an indicator of an evolved planetary system. Therefore, if DZ white dwarfs, which originate from the same stellar population as DZ (Farihi et al. 2011), have a significantly different distribution of magnetic fields, then this would present a compelling case for the CE hypothesis.

(iii) An alternative origin for magnetism among WDs is \( \alpha \omega \) dynamo generation. For a differentially rotating WD with a convective envelope, a magnetic dynamo may be generated at the base of the convection zone (Markiel et al. 1994). However this would be unlikely to produce fields on the order of 1 MG (Thomas et al. 1995), and would lead to magnetic fields strongly aligned with the WD rotation axis which is in general not observed (Latter et al. 1987; Burleigh et al. 1999; Euchner et al. 2002).

5.3 The apparent lack of magnetism in warm DZ

The largest sample of WDs identified in SDSS was presented by Kleinman et al. (2013), using SDSS DR7 spectroscopy. In total they identified 257 DZ, most of which are hotter than the sample we present here (\( T_{\text{eff}} > 8000 \) K), in which case Ca H/K are usually the only metal lines detected. Unlike in cool DZ where the broad wings of the H/K lines absorb most of the flux below 4000 Å (Figure 2), using these lines to detect \( \gtrsim 1 \) MG fields should in principle be a trivial task. Additionally, because of the larger sample size, there is also an abundance of these spectra where the H/K lines have good S/N ratios. We find 64 spectra with S/N > 10 (25 percent), and 27 with S/N > 15 (10 percent).

Inspecting the Ca H/K lines of all 257 DZ did not reveal magnetic splitting for a single object. This is in stark contrast to our fraction of 13 percent. One object, SDSSJ080131.15+532900.8, has what appear to be broadened Ca H/K lines which could indicate a magnetic field. However the SDSS images reveal this WD to be situated \( \sim 7 \) arcsec away from a bright (\( r = 13.6 \)) M star, which likely caused flux contamination in the DZ spectrum (obtained through a 3 arcsec fibre).

The lack of any magnetic DZ in this sample either suggests a different set of selection effects at work in the Kleinman et al. (2013) and our own, or that the incidence of magnetic fields in DZ differs above and below 9000 K. The selection procedure used by Kleinman et al. (2013) was distinctly different to the methodology we employed (§3.1). They fitted DZ templates to a sample of WD candidate spectra, and so magnetic objects will have evaded detection if Zeeman split lines strongly affected the \( \chi^2 \) of their fits.

We performed an independent check by inspecting the warm DZ identified from SDSS DR10 by Gentile Fusillo et al. (2014, submitted). They selected candidate WDs from a colour-cut in the \( (u-g) \) vs. \( (g-r) \) plane situated above the main sequence compared to our cut in Figure 4 and making use of proper-motions. All spectroscopic objects with \( g < 19 \) bounded by this cut were visually inspected and classified into the various WD subclasses. We inspected the H/K lines of all objects classed as DZ for
splitting. Again, of the 118 unique objects, we did not find a single star that can be convincingly claimed to be magnetic. Since the \cite{Gentile Fusillo et al. 2014, submitted} sample were only selected by colour and proper-motion, they are not biased against finding magnetic DZ as \cite{Kleinman et al. 2013} might be.

\cite{Kepler et al. 2013} have recently published a list of new WDs from SDSS DR10 spectra including 397 objects classified as DZ (where most have $T_{\text{eff}} > 10000$ K). Inspecting these 397 spectra reveals \cite{Kepler et al. 2015} have independently discovered 4 of the WDs that we have shown are magnetic (SDSS0735+2057, SDSS0832+4109, SDSS1003−0031, and SDSS1536+4205), however, beyond these, we found no further magnetic objects.

The dearth of MWDs with $T_{\text{eff}} > 8000$ K in the above 3 samples may suggest that magnetic fields are preferentially generated several Gyr after leaving the main-sequence, at least for WDs with evolved planetary systems. If this is the case, then the origin of these fields remains a difficult question to answer. We speculate that the gas giant/CE scenario \cite{Gentile Fusillo et al. 2014, submitted}, previously proposed to occur on the AGB \cite{Nordhaus et al. 2011, Farhi et al. 2011}, may still remain a viable possibility at long WD cooling times. \cite{Veras et al. 2013} and \cite{Mustill et al. 2014} have performed simulations indicating that planet-planet scattering can still occur many Gyr after stellar evolution to the WD stage, and show that these scattered planets will in some cases collide with central star. We suggest such a collision with a scattered gas giant might lead to magnetic field generation. However this scenario has two problems: the small fraction of systems that \cite{Veras et al. 2013} and \cite{Mustill et al. 2014} expect this to occur for in comparison to our magnetic incidence lower limit of $13 \pm 4$ percent, and the lack of hydrogen lines observed in of the spectra in Figure 4.

5.4 Comparison with magnetic DAZ

For cool DZ we arrive at a magnetic incidence of $13 \pm 4$ percent. Yet if we compare this against DAZ WDs, the result is very different. In fact very few magnetic DAZ are known at all, and their magnetic fields are not nearly as strong as found among the DZ in this study. \cite{Kawka et al. 2007} list all magnetic WDs known up to June 2006. Among these are the 3 previously known magnetic DZ (SDSS0157+0033, SDSS1214−0234, SDSS1330+3029). However, not a single magnetic DAZ was known at that time.

Since then, 4 magnetic DAZ have been identified, all with $T_{\text{eff}} < 8000$ K \cite{Farhi et al. 2011, Zuckerman et al. 2011, Kawka & Vennes 2011, 2014}, and with the most magnetic (NLTT 10480) possessing a field of only 0.5 MG \cite{Kawka & Vennes 2011}. As with DZ \cite{5.3}, all known magnetic DAZ have $T_{\text{eff}} > 8000$ K, again suggesting field generation late on the WD cooling track.

Additionally, the fact that cool DAZ are not found with the same regime of magnetic field strengths as DZ is somewhat surprising as they will have similar cooling ages, and so the magnetic field distribution would be expected to be the same, assuming similar progenitors.

One possible explanation is that because metal lines in DAZ appear weaker for a given metal abundance compared with DZ, magnetic splitting of these lines will smear them out in the continuum. Therefore strongly magnetic DAZ would instead be classified as magnetic DA (where the magnetic field can still be inferred from the Balmer series). Higher S/N spectra may reveal known magnetic DA WDs to also be metal polluted.

It is also worth noting that, to date, there are no known magnetic DBZ. This is rather peculiar considering that metals produce stronger lines in atmospheres dominated by helium than those dominated by hydrogen, which should easily allow the detection of fields up to a few MG.

5.5 Field topology

Our results from \cite{5.3} showed that an offset dipole topology provides a reasonable explanation for the minimal magnetic broadening seen in the Zeeman lines of some of the WDs shown in Figure 4.

In this scenario, SDSS1536+4205 has a dipole offset away from the Earth leading to the distribution of observed field strengths appearing sharply peaked at 9.59 MG. It follows from this model that the opposite, invisible hemisphere of the star exhibits a large gradient in field strengths with a strongly magnetic spot ($\sim 50$ MG) emerging at the pole. If the sign of $a_z$ was reversed, the strong gradient in the field across the visible hemisphere would have major observational consequences. The $\sigma$ components in the Mg and Na triplets would be magnetically broadened to the extent of reducing their depth to only $\sim 15$ percent of the $\pi$ component. Therefore, identifying the magnetic nature of the star would require a S/N ratio of at least 40 (for a $3\sigma$ detection).

If the offset dipole model is the correct interpretation for the narrow Zeeman lines, this has a profound consequence for the incidence of magnetism in cool WDs. As discussed above, of these 10 MWDs in our sample, SDSS0157+0033, SDSS1003−0031, SDSS1536+4205, and SDSS2325+0448 all have Zeeman triplets that could arguably be explained by the offset dipole model. If cool MWDs have a tendency for their dipoles to be offset, and if all 4 of the above stars are viewed with their dipoles offset away from us, then statistically this implies that several of the other WDs within our full sample should have dipoles offset towards the Earth. The $\sigma$ components of their Zeeman lines would be broadened to the point that they cannot be distinguished at the low S/N of the SDSS spectra, and so they would not been identified as magnetic. Thus, if true, the offset dipole scenario increases the selection bias against identifying magnetism in cool WDs.

An alternative explanation for the narrowness of the Zeeman lines could also come from a non-uniform distribution of metals across the surface of the WD. If for instance the accreted material accumulated at the poles, the resulting spectrum would exhibit splitting consistent with only the polar field strength. However, to reproduce the minimal magnetic broadening we observe, the metals would have to be constrained to such a small region that the resulting Zeeman triplets would have negligible depths. Alternatively, metals confined to the magnetic equator would also produce a spectrum showing a small range of field strengths, but would be able cover a much greater portion of the visible surface without significant magnetic broadening. However, equatorial accretion would necessitate at least a quadrupolar field.
considered accretion of metals onto a MWD. If the sublimation radius of the WD is smaller than the Alfvén radius (true for our MWD sample), then material is expected to accrete along the magnetic field lines as soon as it enters an ionised state. However, [Metzger et al. (2012)] also discuss a potential caveat to this scenario. The presence of dust grains mixed within the gaseous disc may inhibit the ionisation of the gas component, and so even a strong magnetic field may have little influence over the accretion flow of rocky debris.

It is possible to distinguish between the two scenarios of non-uniform metal accretion and an offset dipole by considering the rotation of magnetic WDs. [Brinkworth et al. (2013)] showed that isolated magnetic WDs have typical rotation periods of hours to days. Many of the WDs they observed in their sample have effective temperatures that fall into the range we study here. In general the magnetic axis of MWDs are not aligned with the rotation axis [Latter et al. (1987); Burleigh et al. (1999); Euchner et al. (2003)], therefore by taking spectra at multiple epochs, one would expect to see variation in the Zeeman line profiles of these stars.

For non-uniformly distributed metals, the projected area of the metal-polluted region would phase with the rotation period. Spectroscopically, this would be seen as a reduction in depth of all Zeeman lines in the triplet proportional to the change in projected area.

For an offset dipole, the effect of rotation would be to bring more/less of the concealed, highly-magnetised pole into view, leading to increased/decreased broadening of the $\sigma$ components of the Zeeman triplet. However the $\pi$ component would remain unchanged in depth.

6 SUMMARY

We have identified a sample of 79 DZ with $T_{\text{eff}} < 9000$ K of which at least 10 possess magnetic fields in the range 0.5–10 MG. This implies a minimum incidence of 13 ± 4 percent which is substantially higher than for young hot DAs. Accounting for various sources of bias, such as poor signal-to-noise spectra and that these objects are identified from a magnitude limited sample, suggests that the true incidence of magnetism in cool DZ is almost certainly higher. We also note the narrowness of the Zeeman lines in several of these objects and show that these are most likely the result of a complex field topology such as an offset dipole. The simultaneous release of SDSS DR11 and DR12 will provide a plethora of new DZ spectra from which improved statistics can be calculated.

ACKNOWLEDGEMENTS

M.H. gratefully acknowledges N. Gentile Fusillo for use of his SDSS spectroscopic catalogue, and T. Marsh for informative discussions on MCMC fitting.

This work makes use of data from SDSS. Funding for SDSS-III has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Science Foundation, and the U.S. Department of Energy Office of Science. The SDSS-III web site is http://www.sdss3.org/.

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