Rho Electroproduction and the Hadronic Contribution to Deeply Virtual Compton Scattering

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Abstract

A two-gluon-exchange model incorporating perturbative and non-perturbative effects is presented for $\rho$ electroproduction which provides an excellent description of all current data. This is then used to calculate the contribution from the $\rho$ to deeply virtual Compton scattering via the vector-meson-dominance transition $\rho \to \gamma$. This is found to be sufficiently large to provide a significant contribution through interference with the perturbative QCD term.
1 Introduction

There is considerable evidence in $\gamma^*p$ reactions that the nominally perturbative regime can be strongly influenced by non-perturbative effects. This is an obvious feature of recent dipole models of deep inelastic scattering [1, 2, 3], where for transverse photons especially the contribution from large (non-perturbative) dipoles extends to significantly large values of $Q^2$. The penetration of non-perturbative physics into the perturbative regime is even more explicit in generalised vector dominance models [4] or in two-component models [5, 6, 7, 8, 9, 10] which combine “soft” (non-perturbative) and “hard” (perturbative) contributions. Typically the soft contribution comprises the normal reggeon and soft pomeron exchanges, the latter with an intercept of $\sim 1.08$. The hard contribution may be a second pomeron, the hard pomeron, with an intercept of $\sim 1.19$ at $Q^2 = 20$ GeV$^2$. In section 2 we present a two-component model for $\rho$ electroproduction which successfully describes all current data. We base our calculations on two-gluon-exchange models of the pomeron. For the non-perturbative contribution we use the model of Diehl [13] and for the perturbative contribution that of Martin, Ryskin and Teubner [14]. The procedure follows the suggestion of [14] by calculating the light quark anti-quark pair $u\bar{u}$ and $d\bar{d}$ production process $\gamma^*p \rightarrow q\bar{q}p$ with the invariant mass of the $qq$-pair $M_X$ afterwards integrated over the mass interval of the $\rho$. This approach has the benefit of avoiding vector meson wave function complications, which can be serious [15], and allows one to concentrate on the production dynamics.

A related topic is that of Deeply Virtual Compton Scattering (DVCS) on protons, $\gamma^*p \rightarrow \gamma p$, which is seen as an important reaction for the study of diffraction in QCD. In the standard QCD approach the amplitude is described by skewed parton distributions [16] corresponding to operator products evaluated between protons of unequal momenta. These are generalizations of the familiar parton distribution of deep inelastic scattering, and like them satisfy perturbative evolution equations [17] which enable them to be evaluated at all $Q^2$ in terms of an assumed input at some appropriate $Q^2_0$. Preliminary data [18] have been presented which are consistent with QCD predictions [19], subject to two uncertainties.

The first is that the theoretical predictions refer to zero momentum transfer $t = 0$ and to compare with experiment, one must integrate over $t$. This is done by assuming an exponential dependence $\exp(-bt)$ and estimating the unmeasured slope parameter $b$. The considerable uncertainty in $b$ leads to a corresponding uncertainty in the normalization of the predictions.

Secondly, it is necessary to specify the input skewed parton distributions at the reference $Q^2_0$. In [19] these are obtained by estimating their ratio to “ordinary” parton distributions

\[ 7 \leq b \leq 10 \text{ GeV}^{-2} \]

\[ ^1 \text{In analysing their preliminary data, H1 [18] assume} \]
at $Q_0^2 = 2.5\,\text{GeV}^2$ using arguments based on the aligned jet model [20], which in practice is almost identical to the simplest diagonal generalized vector meson dominance model for the soft pomeron term [21]. The resulting ratio is of the order of 2, leading to a factor of order four in the predicted DVCS cross-sections. While this provides a reasonable first estimate, it is clearly subject to uncertainties which will become important when more accurate data are available.

Here we note that there are direct “hadronic” contributions to DVCS via the vector-meson-dominance mechanism $\gamma^* p \to V p$, $V \to \gamma$. One particular vector-meson contribution to DVCS, namely that of the $\rho$, can be calculated with reasonable precision using the results of Section 2. This is done in section 3, where we show that the results provide useful constraints on models used to estimate the skewed parton distributions at the reference $Q_0^2$.

2 Rho electroproduction

According to the factorisation theorem [22] the exclusive vector meson production processes can be factored into three parts: the fluctuation of the (virtual) photon into a $q\bar{q}$-pair; the interaction of the $q\bar{q}$-pair with the proton; and the formation of the vector meson from the $q\bar{q}$-pair. Similarly, the upper part of either diagram in figure 1, containing the process $\gamma^* \to q\bar{q}$, can be considered separately from the rest of the diagram. Apart from the couplings $\alpha_s$, the upper parts of the non-perturbative and perturbative diagrams are identical. The lower parts, that is the parts containing the gluons and the proton, are described differently in each approach. The model of Diehl [13] follows Landshoff and Nachtmann (LN) [23]. The gluons are assumed not to interact with each other and a non-perturbative gluon propagator [13] is used:

$$D_{np}(-k^2) = N_{np} \left[ 1 + \frac{k^2}{(n-1)\mu_0^2} \right]^{-n},$$

with $n = 4$. The normalisation $N_{np}$ is determined from the condition

$$\int_0^\infty dk^2 \left[ \alpha_S^{(0)} D_{np}(k^2) \right]^2 = \frac{9\beta_0^2}{4\pi}. \tag{2}$$

The phenomenological parameters $\beta_0$, which describes the effective coupling of the pomeron to the proton, and $\mu_0$ are determined from the total $pp$ and $p\bar{p}$ cross section data and from deep inelastic scattering: $\beta_0 \approx 2.0\,\text{GeV}^{-1}$ and $\mu_0 \approx 1.1\,\text{GeV}$ [24]. For the non-perturbative couplings of the gluons to the quarks forming the $\rho$ a value $\alpha_S^{(0)} \approx 1$ is taken.

It has been argued [23] that the diagrams in which the non-perturbative gluons couple to different valence quarks in the proton are suppressed and therefore can be disregarded. Only the diagrams where both gluons couple to the same valence quark are calculated. Each of the three valence quarks is incorporated into the proton according to the Dirac form factor of the
proton $F_{1p}(t)$, where $t = \Delta^2$ and the four-momenta of the particles are as depicted in figure 1. The energy dependence due to the soft pomeron comes via a factor $x_F^{-\alpha_S(t)}$ in the amplitude, with $x_F \equiv (M_X^2 + Q^2 - t)/(W^2 + Q^2 - m_{proton}^2)$ and $\alpha_S(t)$ the soft pomeron trajectory [23]. In principle we can calculate the $t$-dependence of the soft-pomeron contribution from this, but as this cannot be done for the perturbative contribution, we calculate only at $t = 0$ and use the experimental slope to give the integrated cross section.

Following the argument of [13], the coupling $\alpha_s$ at three of the four vertices is taken at a non-perturbative scale, i.e. $\alpha_s^{(0)}$ is used, while for the vertex where the gluon couples to the off-shell quark it is taken at a perturbative scale $\lambda^2 = (\ell^2 + m_q^2) (Q^2 + M_X^2)/M_X^2$, which is a typical scale for the whole upper part of the diagram.

In the perturbative approach by Martin et al. [14] the pomeron is modelled as a pair of perturbative gluons with symmetric momenta. The perturbative gluon propagator $D_p(k^2) = 1/k^2$ is used. In principle the gluon flux can be obtained from the unintegrated gluon density $f(x_F, |k^2|)$, which gives the probability of finding a $t$-channel gluon with the momentum squared $|k^2|$ in the proton. However, a special treatment of the infrared region is required as the unintegrated gluon density $f(x_F, |k^2|)$ is theoretically undefined as $|k^2| \to 0$ and numerically unavailable below some value of $|k^2| = Q_0^2$, which varies with the parton distribution chosen and usually is in the region from 0.2 to a few GeV$^2$. The linear approximation as suggested in
is used to account for the contribution to the integral from the $|k^2| < Q_0^2$ region. A number of gluon distributions were tried, including MRS(R1), MRS(R2), GRV94HO, GRV94LO and others using the PDFLIB program libraries [26] for numerical calculations. However, the one which gave the best energy dependence within the model is CTEQ4LQ [27], so results are presented only for that choice.

The derivations of both models can be expressed in a common kinematical framework, taking into account the on-shell conditions along the cut line in figure 1, which result in the gluon momenta being predominantly transverse with respect to the $\gamma^*p$ axis, $|k^2| \approx k_t^2$. Here and subsequently transverse two-vectors are shown in bold. Integrating over the azimuthal angles, one obtains a common structure for both models [28] at $t = 0$:

$$\frac{d^2\sigma^{L,Tr}}{dM_X^2dt} = \frac{16e^2\alpha_{em}}{3} \frac{1}{M_X^2} \int_0^{\frac{4M_X^2-m_q^2}{1-4(\ell_i^2+m_q^2)/M_X^2}} \frac{d\ell_i^2}{(\ell_i^2+m_q^2)^2} \left( \frac{\ell_i^2 + m_q^2}{M_X^2} \right) S^{L,Tr}$$

with

$$S^L = 4Q^2 \left( \frac{\ell_i^2 + m_q^2}{M_X^2} \right)^2 \left[ \int \frac{d\ell_i^2}{\ell_i^2} \mathcal{P} \left( \frac{1}{Q^2 + \ell_i^2} - \frac{1}{\sqrt{(Q^2 + \ell_i^2 + k_t^2)^2 - 4k_t^2\ell_i^2}} \right) \right]^2$$

$$S^{Tr} = \left[ \int \frac{d\ell_i^2}{\ell_i^2} \mathcal{P} \left( \frac{1}{Q^2 + \ell_i^2} - \frac{1}{2\ell_i^2} + \frac{Q^2 - \ell_i^2 + k_t^2}{2\ell_i^2\sqrt{(Q^2 + \ell_i^2 + k_t^2)^2 - 4k_t^2\ell_i^2}} \right) \right] \ell_i^2 \left( 1 - \frac{2(m_q^2 + \ell_i^2)}{M_X^2} \right) \left( \frac{M_X^2}{\ell_i^2 + m_q^2} \right)^2 m_q^2 S^L$$

where $Q^2 \equiv m_q^2 + Q^2 \left( \ell_i^2 + m_q^2 \right) / M_X^2$ and the symbol $\mathcal{P}$ denotes the model-dependent parts

$$\mathcal{P}_{np} = F_{1p}(0) x_f^{1-\alpha_S(0)} \left[ \alpha_s(0) \right]^{3/2} \sqrt{\alpha_s(\lambda^2)} \left[ \mathcal{D}_{np} \left( -k_t^2 \right) \right]^2$$

$$\mathcal{P}_p = \frac{\pi}{4} \alpha_s \left( k_t^2 \right) f \left( x_f, k_t^2 \right) \frac{1}{k_t^2}.$$  

Here $f(x_f, k_t^2)$ is related to the gluon distribution $g(x_f, Q^2)$ by

$$x_f g(x_f, Q^2) = \int Q^2 \frac{d\ell_i^2}{k_t^2} f(x_f, k_t^2)$$

with the inverse

$$f(x_f, k_t^2) = k_t^2 \frac{\partial (x_f g(x_f, k_t^2))}{\partial k_t^2}.$$
Such a common structure should be present since both models describe the same physical process. The common parts originate mainly from the kinematics of the process. The difference is contained in equations (6) and (7), arising from the different physical interpretations of the internal dynamics of the process in the two models.

The relation between the models can formally be written as a replacement $P_{np} \leftrightarrow P_p$. There are no $\sqrt{\alpha_s}$ couplings for the two bottom vertices in the perturbative case since the gluons are considered as part of the proton and described by $f(x_p, k_t^2)$. A minor difference is the different argument of $\alpha_s$ in both models and the fact that there is no need for the linear approximation in the nonperturbative model since the integration over the gluon momentum can be performed down to zero. The expressions above are given in a general form but can be further simplified for the light quarks assuming $m_q = 0$.

The forward differential cross section $d\sigma/dt|_{t=0}$ can be related to the total cross section $\sigma(W, Q^2)$ using the experimentally measured forward diffractive slope $b_\rho(Q^2)$ assuming an exponential $t$-dependence of $d\sigma/dt$:

$$\sigma_{\gamma^* p \to \rho p} \simeq \frac{1}{b_\rho(Q^2)} \sum_{q=u,d} \int_{M_1^2}^{M_2^2} dM_X^2 \left[ \varepsilon_{expt} \frac{d\sigma_{\gamma^* p \to q \bar{q} p}}{dt dM_X^2} + \frac{d\sigma_{\gamma^* p \to q \bar{q} p}}{dt dM_X^2} \right]_{t=0}. \quad (10)$$

The slope parameter $b_\rho(Q^2)$ varied from 7 at the smallest $Q^2$ to 4 at the highest $Q^2$. The $M_X^2$-integration limits $M_1^2 = (0.6 \text{ GeV})^2$ and $M_2^2 = (1.05 \text{ GeV})^2$ were chosen to span the $\rho$-region, following [14]. The polarisation of the photon beam $\varepsilon_{expt}$ is a known characteristic of the experiment. For HERA $\varepsilon_{expt} \approx 1$ while for fixed-target experiments it varies significantly, depending on the energy and photon virtuality. It is generally in the range of 0.5 to 0.9 and this is taken into account when comparing our results with the data.

Neither model by itself can describe all the observed features of the $\rho$ electroproduction data simultaneously: that is, the absolute value of the total cross section $\sigma(W, Q^2)$; its dependencies on $Q^2$ and $W$; and the variation of the longitudinal to transverse cross section ratio $R = \sigma_L/\sigma_T$ with $Q^2$. The non-perturbative approach gives an energy dependence which is too flat at the higher values of $Q^2$ due to the soft pomeron intercept while the energy dependence of the perturbative approach, coming from the energy dependence of the gluon density, is clearly too steep at all $Q^2$. The perturbative model does not replicate the $Q^2$-dependence of the NMC data, and the non-perturbative model gives a longitudinal to transverse ratio which is somewhat low\(^\dagger\).

The results of summing the perturbative and non-perturbative production amplitudes

$$\mathcal{P} = \mathcal{P}_{np} + \mathcal{P}_p \quad (11)$$

with $\mathcal{P}_{np}$ and $\mathcal{P}_p$ as given by (5) and (6), are shown in figures 2, 3 and 4 together with the data. It is clear that the two-component model gives excellent agreement. The effect of the value of $Q_0^2$ is shown in figure 2. The effect is consistent both at high and low energy and allows us to fix $Q_0^2 \approx 0.9 \text{ GeV}^2$, which is a reasonable value.

\(^\dagger\)For further details, see [28]
Figure 2: The dependence of total cross section on $Q^2$ compared with high energy data from H1 [12] and ZEUS [11, 31, 32], and low-energy data from NMC [33].

Figure 3: The $Q^2$-dependence of the longitudinal to transverse ratio compared with high energy data from H1 [12, 34, 35] and ZEUS [11, 32, 36], and low energy data from CHIO [37], E665 [38] and NMC [33].

Figure 4: $W$-dependence compared with data from H1 [12], ZEUS [11] and NMC [33]. The use of the open and filled markers is only to indicate to which value of $Q^2$ the data points belong.
3 Deeply virtual Compton scattering (DVCS)

We now use the results of the previous section to estimate the contribution to DVCS from the mechanism of figure 5 and then comment on its implications for the estimation of the skewed parton distributions at the reference $Q^2_0 = 2.6\,\text{GeV}^2$.

3.1 Estimating the $\rho$ contribution

Assuming $s$-channel helicity conservation, only transverse photons contribute to the DVCS cross section. The relation between the DVCS and the $ep \to e\gamma p$ cross sections is

$$
\frac{d^2\sigma_{ep\to e\gamma p}}{dW\,dQ^2} = \frac{\alpha_{\text{em}}}{\pi} \frac{W}{Q^2 \left(W^2 + Q^2 - m^2_{\text{proton}}\right)} \left[1 + (1 - y)^2\right] \sigma_{\gamma^*p \to \gamma p},
$$

(12)

with $y \equiv \left(W^2 + Q^2 - m^2_{\text{proton}}\right) / \left(s - m^2_{\text{proton}}\right)$, $\sqrt{s}$ is the centre-of-mass energy of the $ep$ system and $W$ is that of the $\gamma^*p$ system. The contribution from the mechanism of figure 5 is then given by

$$
\sigma_\rho(\gamma^*p \to \gamma p) \approx \frac{4\pi\alpha_{\gamma}}{\gamma^2_\rho} \sigma(\gamma^*p \to \rho p).
$$

(13)

The coupling $e/\gamma_\rho$ of the $\rho$ to the photon is directly related to the width of the decay $\rho \to e^+e^-$. In the narrow-width approximation

$$
\frac{4\pi}{\gamma^2_\rho} = \frac{3\Gamma_{\rho\to e^+e^-}}{m_\rho \alpha^2} = 0.494 \pm 0.023
$$

(14)

where the experimental values of $m_\rho$, $\Gamma_\rho$ and the branching ratios have been used.

The values obtained from (12), (13) and (14) for the differential cross section $d\sigma_\rho/dQ^2$, averaged over each $Q^2$-bin and integrated over $30\,\text{GeV} < W < 120\,\text{GeV}$ are shown in Table 1, together with the preliminary experimental values for $d\sigma/dQ^2$ with the Bethe-Heitler term.

Figure 5: The hadronic contribution to DVCS arising from a virtual \( \rho \) in the final state.
subtracted off. As calculated, the amplitude in the model is purely imaginary\[1\]. We also give the estimate

\[ R_A(Q^2) = \frac{\mathcal{A}_\rho(\gamma^*p \rightarrow \gamma p)}{\mathcal{A}(\gamma^*p \rightarrow \gamma p)} \approx \left[ \frac{d\sigma_\rho/dQ^2}{d\sigma/dQ^2} \right]^{1/2} \]  

(15)

of the amplitude of figure 5 to the total non-Bethe-Heitler amplitude. As can be seen, this reduces from of order 20 % in the lowest \( Q^2 \) bin to of order 10 % in the highest. Although small, this is not a negligible contribution to the total amplitude for DVCS, since it will interfere constructively with the remaining dominant contributions assuming they are mainly imaginary. It is also worth noting that even for the lowest \( Q^2 \) bin, \( \mathcal{A}_\rho(\gamma^*p \rightarrow \gamma p) \), which one might expect to be predominantly “soft”, contains a significant contribution, about 40 %, from the perturbative term.

| \( Q^2 \) bin [GeV\(^2\)] | \( d\sigma_\rho/dQ^2 \) [pb/GeV\(^2\)] | \( d\sigma_{\text{expt}}/dQ^2 \) [pb/GeV\(^2\)] | \( R_A \) |
|-------------------------|-----------------|-----------------|--------|
| 2.0 to 4.0 | 1.576 | 47±12 \( ^{+10}_{-10} \) | 0.18±0.02 \( ^{+0.02}_{-0.02} \) |
| 4.0 to 6.5 | 0.213 | 6.5±1.6 \( ^{+2.5}_{-2.5} \) | 0.18±0.04 \( ^{+0.04}_{-0.04} \) |
| 6.5 to 11.0 | 0.0352 | 2.10±0.51 \( ^{+0.64}_{-0.64} \) | 0.13±0.02 \( ^{+0.02}_{-0.02} \) |
| 11.0 to 20.0 | 0.00498 | 0.35±0.17 \( ^{+0.14}_{-0.14} \) | 0.12±0.02 \( ^{+0.02}_{-0.02} \) |

Table 1: Comparison of the preliminary experimental values of \( d\sigma/dQ^2 \) after subtraction of the Bethe-Heitler contribution, integrated over 30 GeV < \( W < \) 120 GeV, with the hadronic contribution of figure 5. The corresponding ratio of amplitudes \( R_A \) is also given, assuming the amplitudes are pure imaginary.

### 3.2 Estimating the input distributions

In [19] the input skewed parton distributions at the reference \( Q^2_0 = 2.6 \) GeV\(^2\) were estimated by relating them to “ordinary” parton distributions by using arguments based on the aligned jet model [20]. In practice this is almost identical to the application of generalised vector meson dominance (GVD) in its diagonal form [21]. Both models assume that for the scattering of virtual photons the amplitude at \( t = 0 \) is of the form

\[ \text{Im} \mathcal{A}(\gamma^*N \rightarrow \gamma^*N)_{t=0} = \frac{\alpha}{3\pi} \int_{m_0}^{\infty} dm^2 \frac{m^2 \rho(m^2)}{(Q^2 + m^2)^2} \]  

(16)

\[ ^4 \]There is no interference term, since the data are integrated over the azimuthal angle \( \phi_\gamma \). (See eqn.(40) of [19])

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where $\rho(m^2)$ is taken to be energy independent, corresponding to soft Pomeron behaviour with intercept $\alpha_\rho = 1$. For the aligned jet model $\rho(m^2)$ is given by

$$
\rho(m^2) = \sigma_{AJM}^{\text{Tot}}(m^2) ke^{-e^-(m^2)} \frac{3\langle k_T^2 \rangle}{m^2}.
$$

In [14] the product $\sigma_{AJM}^{\text{Tot}}(k_T^2) ke^{-e^-(m^2)}$ is assumed to be a constant. For diagonal vector meson dominance $\rho(m^2)$ is given by

$$
\rho(m^2) = \sigma_{Vp}^{\text{Tot}}(m^2) \langle k_T^2 \rangle \frac{1}{m^2},
$$

and the identification of the two approximations is completed by the usual diagonal GVD assumption that $\sigma_{Vp}^{\text{Tot}}(m^2) \sim 1/m^2$ for $\alpha_\rho = 1$ and $ke^{-e^-(m^2)}$ is constant.

In the case of DVCS the imaginary part of the amplitude for $t = 0$ is obtained from (16) by replacing one of the propagators with $1/m^2$. Since $m^2 \rho(m^2)$ in (16) and in its DVCS equivalent is taken to be constant in the aligned jet/GVD model, the integrals are trivial, giving the result

$$
\text{Im} \ A(\gamma^* N \rightarrow \gamma N)_{t=0} = \frac{1}{Q^2} (m_0^2 + Q^2) \ln(1 + Q^2/m_0^2).
$$

For a reasonable choice of the lower limit $m_0^2$ in (19), typically 0.4 to 0.6 GeV$^2$, the ratio $\rho$ for $Q^2 \approx 2.5$ GeV$^2$. So knowing $F_2(x, Q^2)$ this gives the input to the DVCS evolution equations [19].

At this point we notice that the same aligned jet/GVD model also implies values for the $\rho$ contribution to DVCS. Attributing the low mass contribution to the $\rho$-meson, one easily obtains

$$
R_A(Q^2) = \frac{\text{Im} \ A(\gamma^* N \rightarrow \gamma N)_{t=0}}{\text{Im} \ A(\gamma^* N \rightarrow \gamma N)_{t=0}} = \frac{\ln(1 + Q^2/M_1^2) - \ln(1 + Q^2/M_2^2)}{\ln(1 + Q^2/M_1^2)}
$$

where we have chosen $m_0^2 = M_1^2 = (0.6 \text{ GeV})^2$ and $M_2^2 = (1.05 \text{ GeV})^2$ for consistency with our treatment of the $\rho$ in Section 2 (cf. equation [10]. This gives values for $R_A$ of 0.43 at $Q^2 = Q_0^2 = 2.6$ GeV$^2$ reducing to 0.28 at $Q^2 = 15$ GeV$^2$. These values are considerably larger than the much more reliable estimates of section 3.1.

This discrepancy is not surprising given the extreme simplicity of the aligned jet/GVD model used. More elaborate versions can be constructed and will be required in the future to estimate more accurately the skewed parton distributions at the reference $Q_0^2$. Such models will need to take account of both “hard” and “soft” diffraction, and in constructing them the requirements that they be compatible with the $\rho$ contributions of Section 3.1, as well as the structure function data for $0 \leq Q^2 \leq Q_0^2$, will be essential constraints.
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