Electron–Hole Crossover in Gate-Controlled Bilayer Graphene Quantum Dots

L. Banszerus,* A. Rothstein, T. Fabian, S. Möller, E. Icking, S. Trellenkamp, F. Lentz, D. Neumaier, K. Watanabe, T. Taniguchi, F. Libisch, C. Volk, and C. Stampfer

ABSTRACT: Electron and hole Bloch states in bilayer graphene exhibit topological orbital magnetic moments with opposite signs, which allows for tunable valley-polarization in an out-of-plane magnetic field. This property makes electron and hole quantum dots (QDs) in bilayer graphene interesting for valley and spin-valley qubits. Here, we show measurements of the electron–hole crossover in a bilayer graphene QD, demonstrating opposite signs of the magnetic moments associated with the Berry curvature. Using three layers of top gates, we independently control the tunneling barriers while tuning the occupation from the few-hole regime to the few-electron regime, crossing the displacement-field-controlled band gap. The band gap is around 25 meV, while the charging energies of the electron and hole dots are between 3 and 5 meV. The extracted valley g-factor is around 17 and leads to opposite valley polarization for electrons and holes at moderate B-fields. Our measurements agree well with tight-binding calculations for our device.

KEYWORDS: quantum dot, bilayer graphene, electron–hole crossover

Carbon-based quantum dots (QDs) are attracting attention as promising hosts for spin, valley, or spin-valley qubits. While spin qubits—the central building blocks of spin-based quantum computing—have already been intensively studied in III/V heterostructures and silicon, the valley degree of freedom (where present) has been considered mainly as an undesirable constraint. This is beginning to change, and proposals of valley-based quantum computation have led to the demonstration of spin-valley qubits in carbon nanotubes and more recently in silicon. Bilayer graphene (BLG) could play an important role in this development. Besides the small spin–orbit interaction and the weak hyperfine coupling, the tunability of the valley-dependent topological orbital magnetic moment in gapped BLG offers new knobs for controlling the valley degree of freedom. As the topological orbital magnetic moment is associated with the Berry curvature, it has different signs for the different valleys, as well as for electrons and holes, and causes a large and adjustable effective valley g-factor. In contrast to silicon, where the lifting of the valley degeneracy is set by the confining potential, the large valley g-factor in BLG offers control of the valley splitting and allows us to achieve full valley polarization as a function of magnetic field and quasi-particle index (electrons or holes). This, together with the tunable band gap, makes BLG interesting for the implementation of spin-valley qubits based on electron and hole QDs.

Quantum dots in single-layer and bilayer graphene have been investigated intensively in the past decade. First, QD devices were carved out from individual flakes, which allowed researchers to study excited states spectra, spin states, and charge relaxation. However, these devices were heavily affected by edge disorder, which limited the control over the QD occupation and made it difficult to identify the electron–hole crossover. Recent technological improvements that combine the encapsulation of BLG in hexagonal boron nitride (hBN) with a graphite back gate have opened the door to gate-controlled quantum point contacts and QDs. Excited state spectroscopy, charge detection, and single-electron occupation of single and double QDs have been shown for such BLG quantum devices. Common to all these devices is that a set of gates (the so-called split gates) is used to form either a p-doped or n-doped channel in which an additional finger gate forms a p-n-p or n-p-n band profile. The two naturally occurring pn-junctions serve as tunneling barriers of the gated-defined QD. This technology, however,
limits the control of the tunneling rates and requires the QD to have the opposite polarity as the neighboring reservoirs.\textsuperscript{27,27}−\textsuperscript{32} The lack of independent control of the dot occupation explains why it has remained a challenge to demonstrate the direct transition from the few-electron to the few-hole regime (as in carbon nanotube QDs\textsuperscript{33,34}) in BLG QD devices. Here, we report on the observation of the electron−hole crossover in a gate-defined bilayer graphene QD by independently controlling the tunneling barriers and the dot occupation. Two dedicated finger gates induce two tunneling barriers in a split-gate defined channel and define a single QD between the barriers. The electrochemical potential of the QD can then be independently controlled by a third finger gate. Thanks to the small band gap in BLG, moderate gate voltages allow the tuning of the QD from the few-hole regime through the band gap into the few-electron regime. Finite-bias spectroscopy measurements allow us to determine the energy scales of the system, such as the charging energies (3−5 meV) and the band gap (around 25 meV), which is in good agreement with the applied displacement field. Finally, we show that, when applying an out-of-plane magnetic field, electrons and holes are polarized in different valleys (K\textsuperscript{+} and K\textsuperscript{−}) due to a large valley g-factor but opposite sign of the topological orbital magnetic moment. The experimentally extracted valley g-factor (g\textsubscript{v} \approx 17) is in good agreement with tight-binding calculations.

Figure 1. (a) Scanning electron microscopy image showing the geometry of the QD device. The split gates (SGs) define the conducting channel, which can be modulated by voltages on the finger gates (highlighted by false colors). The ohmic source and drain contact to the BLG are labeled by S and D, respectively. (b, c) Schematic cross sections through the device along different directions (see white arrows in panel (a)). The hBN/BLG/hBN heterostructure rests on a graphene flake, which serves as a back gate (BG) and is placed on a SiO\textsubscript{2}/Si substrate. The gate stack placed on top of the heterostructure consists of three metal (Cr/Au) layers, insulated from each other by Al\textsubscript{2}O\textsubscript{3} layers as a gate dielectric; the SGs are followed by two layers of finger gates, some labeled here as barrier gates (BL, BR; yellow) and the plunger gate (PG; orange). (d) Schematics of the valence and conduction band edge profiles along the p-doped channel illustrating the different regimes (I, II, III, and IV) set by the barrier gate and plunger gate voltages (the darker gray the finger gate is, the higher the applied voltage is). The band edges separate electron (El) and hole (Ho) states. (e) Charge stability diagram showing the conductance as a function of the barrier gate voltages \(V_{\text{BL}}\) and \(V_{\text{BR}}\) at \(V_{\text{PG}} = 0\) V and \(V_{\text{SD}} = 200\) μV. (f) Similar to panel (e) but at \(V_{\text{PG}} = 5\) V. The labels in (e) and (f) correspond to the ones in panel (d); the dashed lines are described in the text, and the black crosses mark the exact same barrier gate voltages.
long channel where the QDs will be formed (see top view in Figure 1a and cross-section along the channel in Figure 1c). This structure is covered by a 25 nm thick layer of atomic-layer-deposited (ALD) Al₂O₃. On top we place the first set of finger gates with a width of 70 nm and a pitch of 150 nm, which later serve as the left and right barrier (BL and BR) gates (see cross-section in Figures 1b,c). Finally, we deposit a second ALD Al₂O₃ layer and place a second set of interdigitated finger gates (again with a width of 70 nm). One of these gates will later be used as a plunger gate (PG). The different metal layers (all Cr/Au) have a thickness of ≈25 nm. All measurements are performed in a 3He/4He dilution refrigerator at a base temperature of 10 mK, using standard DC and low-frequency lock-in (MFLI Zurich Inst.) measurement techniques.

To confine the charge carriers to the 130 nm wide channel connecting the source and drain leads, we open a band gap in the BLG areas below the split gates. This is achieved by applying a transverse displacement field of 0.35 V/nm, which we induce by a back gate voltage of \( V_{	ext{BG}} = -2 \) V and a split gate voltage of \( V_{	ext{SG}} = 2.15 \) V. The displacement field breaks the inversion symmetry of the BLG, resulting in a band gap of around 28 meV 36,37 (see left illustration in Figure 1d,I). Moreover, the similar magnitudes of the applied voltages make sure that below the SGs the Fermi level is within the band gap. The negative BG voltage leads to a p-doping of the channel as there is no SG above the channel for compensating the field-effect-induced charge carrier density. This task, however, can now be performed by the different finger gates, which allow full electrostatic control of the shape of the band profile along the channel as depicted in Figure 1d. For example, while keeping the PG voltage constant (\( V_{	ext{PG}} = 0 \) V), we can use the left and right barrier gate, BL and BR, to pinch-off the current through the channel. In Figure 1e we show a corresponding charge stability diagram, i.e., the conductance (in log-scale) as a function of positive BL and BR voltages (\( V_{	ext{BL}} \) and \( V_{	ext{BR}} \), showing a number of different regimes (see labels). In the lower left corner (regime I) the conductance is on the order of \( e^2/h \) and the Fermi level is throughout the entire channel below the valence band edge (see Figure 1d,I). When increasing the voltages on the left and right barrier gate, we locally push the band edges down in energy such that below BL and BR the Fermi level is within the band gap (see Figure 1d,II). This forms a hole QD (hQD) coupled by two tunneling barriers to the p-doped source and drain reservoirs. In the charge stability diagram a strongly reduced conductance and nearly periodic Coulomb resonances with a slope of around \(-1\) (regime II) appear, meaning that both barrier gates are tuning the QD states equally well. The slightly negative curvature of the Coulomb resonances in the \( V_{	ext{BL}}-V_{	ext{BR}} \) plane (see dashed line in Figure 1e) are typical for gate-defined hole QDs; with increasing voltage at one barrier gate the QD is shifted toward
the other barrier gate, which then couples more strongly, resulting in an overall asymmetric gate coupling.

By keeping the barrier gate voltages fixed (see cross in Figures 1e and 1f) but changing the PG, we can tune the system from a hole QD to an electron QD (eQD) configuration (Figure 1d,III). A corresponding charge stability diagram for $V_{\text{PG}} = 5 \text{ V}$ is shown in Figure 1f. Again, we see Coulomb resonances with a slope of about $-1$ (regime III around the cross in Figure 1f). The spacings of these Coulomb resonances are smaller compared to those of the hQD, which is due to the fact that the eQD is larger than the hQD (compare Figure 1d,II with Figure 1d,III). In addition, a slight positive curvature of the Coulomb resonances is observed in Figure 1f, which fits well with an eQD, by increasing the voltage at one of the barrier gates, the band edges are pushed down locally and the QD shifts exactly in the direction of this gate, which leads to an enhanced gate coupling and an increasing asymmetry in the coupling of BL and BR. Note that even in the case of $V_{\text{PG}} = 0 \text{ V}$ at very high barrier gate voltages ($V_{\text{BL}}, V_{\text{BR}} \gtrsim 5.8 \text{ V}$) an even larger eQD can be formed (see Figure 1e and blue dashed line in Figure 1d,IV). However, when using the barrier gates to tune from this configuration toward the hQD, one passes through a double quantum dot regime consisting of two eQDs (see Figure 1d,IV and regime IV in Figure 1e), highlighting the importance of having the plunger gate for observing the electron–hole crossover in a single QD. Additional charge-stability diagrams for different plunger gate voltages are shown in the Supporting Information (Figure S1).

The crossover from a hole to an electron QD becomes visible at best in the conductance as a function of $V_{\text{PG}}$ at constant barrier gate voltages. Such a measurement is shown in Figure 2a, where the Coulomb peaks of the first 10 holes and the first 10 electrons as well as the BLG band gap can be identified (see labels). To prove the single quantum dot nature of these resonances, we measure in Figure 2b a charge-stability diagram as a function of $V_{\text{PG}}$ and $V_{\text{BR}}$, highlighting two sets of Coulomb resonances with a linear slope (see dashed lines) separated by a gap. This gap separates the hQD from the eQD (see schematic in Figure 2c) and is directly connected to the displacement-field-induced band gap in BLG. The observed slopes of the Coulomb resonances provide the relative lever arm, i.e., the relative gate coupling of the plunger gate with respect to the barrier gate BR. For instance, the plunger gate couples to the hQD about 3.5 times worse than the BR gate (slope of around $-0.28$), which can mainly be explained by the larger vertical distance of the PG (see Figure 1c) and partial screening by the barrier gates. This effect even gets enhanced when tuning to the eQD, where the BR gate couples around 5.5 more strongly than the PG (slope of around $-0.18$), because the eQD is larger and extends more toward the barrier gate (see Figure 1c,III).

To extract energy scales of our system we performed finite bias measurements. In Figure 2d we show corresponding Coulomb-blockade diamond measurements, i.e., measurements of the differential conductance ($G = dI/dV_{\text{SD}}$) as a function of bias voltage $V_{\text{SD}}$ and $V_{\text{PG}}$ for fixed barrier gate voltages (taken in the same regime as the data presented in Figure 2a). A large diamond associated with the band gap separates the hole QD from the electron QD, highlighting the few-hole and the few-electron regime. Here, the first hole and the first electron exhibit lever arms of $a_{1h} = 0.016 \text{ meV/mV}$ and $a_{1e} = 0.009 \text{ meV/mV}$. From the extension of the big diamond, i.e., the intersection of the corresponding charging lines (see dashed lines in Figure 2d), a band gap of $\approx 23.5 \text{ meV}$

Figure 3. (a) Calculated single particle spectrum of a BLG QD with a size of $100 \times 250 \text{ nm}$ as a function of an out-of-plane magnetic field (see text). With increasing field, the electron and hole states become K$^+$ and K$^-$ polarized, respectively. The valleys are assigned by the sign of the orbital magnetic moment (slope). At zero magnetic field, orbital degeneracies are observed (multiplets of colored lines at $B = 0 \text{ T}$). (b) Coulomb peaks reproduced from (a) by adding a charging energy of $3.4 \text{ meV}$ to each single particle eigenstate in order to model the experimental transport data. The 2-fold spin and 2-fold orbital degeneracy (due to the chosen potential) lead to a 4-fold degenerate spectrum. (c) Measured Coulomb resonances in the electron and hole regime as a function of $V_{\text{PG}}$ and an out-of-plane magnetic field, $B$ ($V_{\text{SD}} = 400 \mu\text{V}$). The dashed line is a guide to the eye and the positive/negative slope of holes/electrons as a function of positive B-fields reflects the opposite net valley polarization. (d) Energy shift of the Coulomb resonances (i.e., peaks) in panel (c) with respect to the peak position at $B = 0 \text{ T}$, averaged over the first ten charge transitions for the electron (top) and hole (bottom) regime. The colored lines show the average energy shift of the first ten states obtained from the tight-binding calculation presented in panel (b). The colors of the lines indicate the increasing valley polarization with the color code indicated in the inset.
is extracted. This gap is in agreement with the one estimated from the applied transverse displacement field (see above). The band gap itself appears in this measurement as not completely blocking transport for larger source-drain voltage values. For \( V_{SD} \) values that exceed \( \approx 2.5 \) mV, a background conductance sets in and increases stepwise with \( V_{SD} \). This is not fully understood, but the fact that this background conductance is independent of the plunger gate voltage suggests that it originates from a parallel channel formed under the split gates rather than from transport through the QD.

The Coulomb diamond measurements (Figure 2d) also allow us to determine the addition energies of the first hole, \( E_{add} = 5.3 \) meV, and of the first electron, \( E_{add} = 2.4 \) meV. With the help of the gate lever arms \( a^{1e} \) and \( a^{1h} \) we accordingly extract the QD capacitances of \( C_E = 31 \) aF and \( C_E = 66 \) aF. Using a simplified plate capacitor model consisting of a disk 25 nm above the graphite back gate, we estimate an effective diameter of the hole and electron quantum dot of about 170 and 250 nm, respectively. This is a rather rough estimate, but the order of magnitude is reasonably consistent with the geometry of our device and reflects the different sizes of the hole and electron QD (compare Figures 1d,II and 1d,III).

Next, we show that electrons and holes respond almost mirror-symmetrically to an out-of-plane magnetic field. The Berry curvature \(^3\) near the valley centers \( K^+ \) and \( K^- \) hole and electron QD (compare Figures 1d,II and 1d,III).

The valley polarization can indeed be clearly seen when looking at the single particle spectrum of an electron/hole quantum dot as a function of out-of-plane magnetic field (Figure 3a). Here, we present tight-binding calculations of a BLG QD of experimental dimensions using a finite mass term.\(^\text{41}\) Explicitly, we assume a soft box of dimensions 150 × 200 nm, and we additionally add a cosine and a small linear term to account for a not-perfectly-flat confinement. Moreover, we add a displacement field to open a band gap of \( \Delta = 20 \) meV with on-site terms of \( \pm \Delta /2 \).

At zero magnetic field each orbital state is 4-fold degenerate due to the spin and valley degrees of freedom. Applying an out-of-plane magnetic field causes a valley splitting,\(^\text{42}\) where states from one valley (see, e.g., the green lines in Figure 3a) rapidly increase in absolute energy value (see green and red lines in Figure 3a), while states from the other valley (blue and orange lines) evolve toward the lowest Landau levels. At higher B-fields, a net valley polarization is therefore established for the first QD states (see labels in Figure 3a). This valley polarization is different for electrons (\( K^+ \)) and holes (\( K^- \)).

In order to compare theory with experiment we add to our model a phenomenological charging energy of \( E_C = 3.4 \) meV by shifting the \( n^{16} \) eigenvalue of the single particle Hamiltonian by \( n \cdot E_C \) (see Figure 3b). The model shows not only the band gap but also the different sign of the topological orbital magnetic moment for electrons and holes, expressed by the different sign of the slope of the individual states. The steepness of the slope at high B-field is given by the valley g-factor. Our model can be directly compared to Coulomb resonance measurements recorded as a function of plunger gate voltage and out-of-plane B-field (Figure 3c). We observe that the Coulomb resonances in the hole and in the electron regime shift toward the gap with opposite slopes with increasing out-of-plane magnetic field, in good agreement with Figure 3b. This shift originates from a net valley polarization of the QD due to the large valley g-factor. Although we cannot resolve individual level crossings in the experiment, which is mainly due to the rather large size of the QDs, we observe that for small magnetic fields there is a very low B-field dependence of the QD states. This fits well with the zigzag lines in Figure 3b, which are due to level crossings of states with different valleys (see Figure 3a) showing up as small kinks in Figure 3b. Note that with increasing magnetic field, tunneling through the QD is increasingly suppressed, resulting in lower Coulomb peak amplitudes.

For a quantitative comparison between experiment and theory and for extracting the valley g-factor \( g_v \) we investigate the energy shift of the Coulomb peaks with respect to the peak position at \( B = 0 \) T, averaged over the first ten holes and ten electrons, as a function of B-field (see Figure 3c). The experimental data show an increasing valley polarization, reflected in the increasing energy shift toward lower (higher) values for electron (hole) states, respectively. The colored lines are the result of the same averaging treatment applied to the tight-binding model calculation shown in Figure 3b and are in good agreement with the experiment, highlighting the opposite valley polarization for electrons and holes (see labels and inset in Figure 3c). The maximum extracted \( g_v \) is \( \approx 16 \) for electrons (see dashed line in Figure 3d) and \( \approx 17 \) for holes.

For achieving agreement between theory and experiment it is crucial that in the model system the QD potential is not ‘flat’ but exhibits a sizable zero point energy of a few meV. This is because in a large and ‘flat’ QD the evolution of the lowest Landau level near the band gap would limit the slopes of the lowest individual states to \( g_v \approx 3 \).\(^\text{43}\) This value is in contrast to the maximum extracted \( g_v \) of around 17 which has also been observed in earlier works.\(^\text{59}\) The slightly smaller average valley g-factor in the model compared to that from the experiment might be due to the specific potential shape, strain,\(^\text{44}\) additional valley splitting, or effects which are not captured by the single particle Hamiltonian. The small electron hole asymmetry might be explained by the different QD size for electrons and holes.\(^\text{14}\)

To conclude, we demonstrate the electron–hole crossover in a gate-defined BLG QD by employing a gating scheme where three finger gates independently control the two tunnel barriers and the electrochemical potential of the QD. We tune the occupation of the QD from the few-hole regime across the band gap into the few-electron regime, where the extracted band gap of 23.5 meV is in good agreement with the gap induced by the transverse displacement field. Finally, we show that electrons and holes have different signs of the topological orbital magnetic moments, allowing for different valley polarization at moderate out-of-plane magnetic fields. This, together with the large valley g-factor, makes quantum systems based on combinations of coupled BLG electron and hole quantum dots interesting for valley and spin-valley qubits. For future experiments, implementing a radio frequency charge detector would allow us to study dynamical processes in BLG QDs and help to prove the occupation number of the QD, independently from the tunneling rates.
The authors declare no competing financial interest.
Ensslin, K. Graphene single-electron transistors. *Mater. Today* 2010, 13, 44–50.

(16) Schnez, S.; Molitor, F.; Stampfer, C.; Güttinger, J.; Shorubalko, I.; Ihn, T.; Ensslin, K. Observation of excited states in a graphene quantum dot. *Appl. Phys. Lett.* 2009, 94, 012107.

(17) Volk, C.; Fringes, S.; Terrès, B.; Dauber, J.; Engels, S.; Trellenkamp, S.; Stampfer, C. Electronic Excited States in Bilayer Graphene Double Quantum Dots. *Nano Lett.* 2011, 11, 3581–3586.

(18) Güttinger, J.; Frey, T.; Stampfer, C.; Ihn, T.; Ensslin, K. Spin States in Graphene Quantum Dots. *Phys. Rev. Lett.* 2010, 105, 116801.

(19) Volk, C.; Neumann, C.; Kazarski, S.; Fringes, S.; Engels, S.; Haupt, F.; Müller, A.; Stampfer, C. Probing relaxation times in graphene quantum dots. *Nat. Commun.* 2013, 4, 1753.

(20) Bischoff, D.; Krähenmann, T.; Drösser, S.; Gruner, M. A.; Barraud, C.; Ihn, T.; Ensslin. K. Reactive-ion-etched graphene nanoribbons on a hexagonal boron nitride substrate. *Appl. Phys. Lett.* 2012, 101, 203103.

(21) Engels, S.; Epping, A.; Volk, C.; Korte, S.; Voigtländer, B.; Watanabe, K.; Taniguchi, T.; Trellenkamp, S.; Stampfer, C. Etched graphene quantum dots on hexagonal boron nitride. *Appl. Phys. Lett.* 2013, 103, 073113.

(22) Güttinger, J.; Stampfer, C.; Libisch, F.; Frey, T.; Burgdörfer, J.; Ihn, T.; Ensslin, K. Electron-Hole Crossover in Graphene Quantum Dots. *Phys. Rev. Lett.* 2009, 103, 046810.

(23) Engels, S.; Terrès, B.; Epping, A.; Khodkov, T.; Watanabe, K.; Taniguchi, T.; Beschoten, B.; Stampfer, C. Limitations to Carrier Mobility and Phase-Coherent Transport in Bilayer Graphene. *Phys. Rev. Lett.* 2014, 113, 126801.

(24) Overweg, H.; Eggimann, H.; Chen, X.; Slizovskiy, S.; Eich, M.; Pisoni, R.; Lee, Y.; Rickhaus, P.; Watanabe, K.; Taniguchi, T.; Fal'kò, V.; Ihn, T.; Ensslin, K. Electrostatically Induced Quantum Point Contacts in Bilayer Graphene. *Nano Lett.* 2018, 18, 553–559.

(25) Kraft, R.; Krainov, I. V.; Gall, V.; Dmitriev, A. P.; Krupke, R.; Gorinyi, I. V.; Danneau, R. Valley Subband Splitting in Bilayer Graphene Quantum Point Contacts. *Phys. Rev. Lett.* 2018, 121, 257703.

(26) Banszerus, L.; Frohn, B.; Fabian, T.; Somanchi, S.; Epping, A.; Müller, M.; Neumaier, D.; Watanabe, K.; Taniguchi, T.; Libisch, F.; Beschoten, B.; Hasler, F.; Stampfer, C. Observation of the Spin-Orbit Gap in Bilayer Graphene by One-Dimensional Ballistic Transport. *Phys. Rev. Lett.* 2020, 124, 177701.

(27) Eich, M.; Pisoni, R.; Overweg, H.; Kurzmann, A.; Lee, Y.; Rickhaus, P.; Ihn, T.; Ensslin, K.; Herman, F.; Sigrist, M.; Watanabe, K.; Taniguchi, T. Spin and Valley States in Gate-Defined Bilayer Graphene Quantum Dots. *Phys. Rev. X* 2018, 8, 031023.

(28) Banszerus, L.; Frohn, B.; Epping, A.; Neumaier, D.; Watanabe, K.; Taniguchi, T.; Stampfer, C. Gate-Defined Electron–Hole Double Dots in Bilayer Graphene. *Nano Lett.* 2018, 18, 4785–4790.

(29) Kurzmann, A.; Eich, M.; Overweg, H.; Mangold, M.; Herman, F.; Rickhaus, P.; Pisoni, R.; Lee, Y.; Garreis, R.; Tong, C.; Watanabe, K.; Taniguchi, T.; Ensslin, K.; Ihn, T. Excited States in Bilayer Graphene Quantum Dots. *Phys. Rev. Lett.* 2019, 123, 026803.

(30) Kurzmann, A.; Overweg, H.; Eich, M.; Pally, A.; Rickhaus, P.; Pisoni, R.; Lee, Y.; Watanabe, K.; Taniguchi, T.; Ihn, T.; Ensslin, K. Charge Detection in Gate-Defined Bilayer Graphene Quantum Dots. *Nano Lett.* 2019, 19, 5216–5221.

(31) Banszerus, L.; Möller, S.; Icking, E.; Watanabe, K.; Taniguchi, T.; Volk, C.; Stampfer, C. Single-Electron Double Quantum Dots in Bilayer Graphene. *Nano Lett.* 2020, 20, 2005–2011.

(32) Banszerus, L.; Fabian, T.; Möller, S.; Icking, E.; Heiming, H.; Trellenkamp, S.; Lentz, F.; Neumaier, D.; Otto, M.; Watanabe, K.; Taniguchi, T.; Libisch, F.; Volk, C.; Stampfer, C. Electrostatic Detection of Shubnikov-de-Haas oscillations in Bilayer Graphene by Coulomb Resonances in Gate-Defined Quantum Dots. *Phys. Status Solidi B* 2020, 1.

(33) Jarillo-Herrero, P.; Sapmaz, S.; Dekker, C.; Kouwenhoven, L. P.; van der Zant, H. S. J. Electron-hole symmetry in a semiconducting carbon nanotube quantum dot. *Nature* 2004, 429, 389–392.

(34) Kuemmeth, F.; Ilani, S.; Ralph, D. C.; McEuen, P. L. Coupling of spin and orbital motion of electrons in carbon nanotubes. *Nature* 2008, 452, 448–452.

(35) Wang, L.; Meric, I.; Huang, P. Y.; Gao, Q.; Gao, Y.; Tran, H.; Taniguchi, T.; Watanabe, K.; Campos, L. M.; Muller, D. A.; Guo, J.; Kim, P.; Hone, J.; Shepard, K. L.; Dean, C. R. One-Dimensional Electron-Contact to a Two-Dimensional Material. *Science* 2013, 342, 614–617.

(36) McCann, E. Asymmetry gap in the electronic band structure of bilayer graphene. *Phys. Rev. B: Condens. Matter Mater. Phys.* 2006, 74, 161403.

(37) Slizovskiy, S.; Garcia-Ruiz, A.; Drummond, N.; Falko, V. I. Dielectric susceptibility of graphene describing its out-of-plane polarizability. *arXiv (Condensed Matter, Mesoscopics and Nanoscale Physics)*, December 20, 2019, 1912.10067v1, ver. 1. https://arxiv.org/abs/1912.10067v1 (accessed 2020).

(38) Berry, M. V. Quantal phase factors accompanying adiabatic changes. *Proc. R. Soc. Lond. A* 1984, 392, 45–57.

(39) Xiao, D.; Yao, W.; Niu, Q. Valley-Contrasting Physics in Graphene: Magnetic Moment and Topological Transport. *Phys. Rev. Lett.* 2007, 99, 236809.

(40) Koshino, M. Chiral orbital current and anomalous magnetic moment in gapped graphene. *Phys. Rev. B: Condens. Matter Mater. Phys.* 2011, 84, 125427.

(41) Zhang, F.; Jung, J.; Fiete, G. A.; Niu, Q.; MacDonald, A. H. Spontaneous Quantum Hall States in Chirally Stacked Few-Layer Graphene Systems. *Phys. Rev. Lett.* 2011, 106, 156801.

(42) Kuzmenko, A. B.; Crasse, I.; van der Marel, D.; Blake, P.; Novoselov, K. S. Determination of the gate-tunable band gap and tight-binding parameters in bilayer graphene using infrared spectroscopy. *Phys. Rev. B: Condens. Matter Mater. Phys.* 2009, 80, 165406.

(43) da Costa, D. R.; Zarenia, M.; Chaves, A.; Farias, G. A.; Peeters, F. M. Magnetic field dependence of energy levels in biased bilayer graphene quantum dots. *Phys. Rev. B: Condens. Matter Mater. Phys.* 2016, 93, 085401.

(44) Moulisdale, C.; Knothe, A.; Fal'ko, V. Engineering of the topological magnetic moment of electrons in bilayer graphene using strain and electrical bias. *Phys. Rev. B: Condens. Matter Mater. Phys.* 2020, 101, 085118.

(45) Albrecht, W.; Moers, J.; Hermanns, B. HNF - Helmholtz Nano Facility. *Journal of Large-Scale Research Facilities* 2017, 3, 112.