Holographic free-electron light source

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Recent advances in the physics and technology of light generation via free-electron proximity and impact interactions with nanostructures (gratings, photonic crystals, nano-undulators, metamaterials and antenna arrays) have enabled the development of nanoscale-resolution techniques for such applications as mapping plasmons, studying nanoparticle structural transformations and characterizing luminescent materials (including time-resolved measurements). Here, we introduce a universal approach allowing generation of light with prescribed wavelength, direction, divergence and topological charge via point-excitation of holographic plasmonic metasurfaces. It is illustrated using medium-energy free-electron injection to generate highly-directional visible to near-infrared light beams, at selected wavelengths in prescribed azimuthal and polar directions, with brightness two orders of magnitude higher than that from an unstructured surface, and vortex beams with topological charge up to ten. Such emitters, with micron-scale dimensions and the freedom to fully control radiation parameters, offer novel applications in nano-spectroscopy, nano-chemistry and sensing.
A diverse toolkit of meso-/macroscopic optical elements exists to control and manipulate light, that is, its amplitude, polarization, photon energy and momentum, in free-space and photonic waveguide systems. Recent advances in nanofabrication technologies and improved understanding of near-field light/matter/free-electron interactions are now enabling the extension of such control to the nanoscale: the coupling of light into well-defined free-space modes of photon energy, momentum and polarization has been made possible with the help of photonic crystals, surface waves and photonic metamaterials. Specifically in relation to electron beam excitations, plasmonic nanoantennas and collective oscillating metamolecule ensembles have been engaged to such ends. Regardless of the mode of excitation, structures are typically constrained to controlling the direction and polarization of emitted light.

Holography was originally conceived as a technique for increasing the resolution of scanning electron microscopes, but has come to be widely recognized as the ultimate method of achieving three-dimensional optical reconstruction of objects. In essence, it relies on the encoding of an ‘object’ wavefront in a recorded interference pattern produced with a ‘reference’ wave; the object wave can then be reconstructed by illuminating the interference pattern with the reference wave. Its conceptual simplicity sees the technique employed routinely for wavefront conversion of light and matter waves, where the required interferogram is computationally generated.

In this work, we propose a flexible means of precisely controlling the wavefront of light emanating from a singular nanoscale emitter by locating it in a nanostructured environment designed according to holographic principles (Fig. 1). Surface nanostructures are engineered to convert the divergent transition radiation and surface plasmon polaritons emanating from the impact point of an electron beam on a metal surface into light beams with selected wavefronts, specifically directional plane waves and high-order optical vortex beams.

**Results**

**Holographic design for electron-induced emission control.** A charged particle crossing the boundary between two different media generates transition radiation (TR), with a spectral distribution and intensity related to the relative permittivities of the media and the electron energy. On metal surfaces such impacts also generate surface plasmon polaritons (SPPs).

![Figure 1](image_url)

**Figure 1 | Holographic free-electron light source design.** (a) The electromagnetic excitation resulting from normally incident free-electron impact on a metal surface is computationally replicated by an electric dipole located in close proximity to the surface. The holographic mask required to couple this excitation to a desired output beam is obtained via the interference of the dipole-generated near-field and the required output field, as schematically illustrated for a collimated plane wave at an oblique angle to the surface-normal. (b) Binary version of the as-generated greyscale interference pattern required to produce, from the impact of 30 keV electrons on a gold surface, an output beam at a wavelength of 800 nm directed at 30° to the surface-normal. (c) False colour scanning electron microscope image of the pattern from panel (b) fabricated on an optically thick (140 nm) gold film (scale bar, 10 μm).
propagating radially from the impact point. Indeed, for certain metals at certain frequencies and electron energies the efficiency of coupling to SPPs may be greater than to TR, but SPPs can only contribute to free-space (far-field) light emission in the presence of a decoupling structure such as a grating; TR is otherwise the dominant output component. The TR from an electron normally incident on a metal surface has a cylindrically symmetric toroidal emission pattern (illustrated schematically in Fig. 1a) very similar to that of a dipole aligned with the surface-normal (at a distance from the surface $h \ll \lambda$, where $\lambda$ is the light wavelength). Indeed, for numerical modelling purposes, an electron impact excitation on a metal, including SPP generation, can be accurately represented as such.

We select an emission design wavelength $\lambda = 800$ nm for the present study, which in experiment utilizes 30 keV electrons normally incident on gold surfaces. The corresponding numerically simulated distribution of electromagnetic field in the gold/vacuum interface plane is employed as the ‘reference’ field (in holographic parlance) to generate an interference pattern with an ‘object’ light field corresponding to the desired output wavefront, which by inversion defines the 2D surface structure required to regenerate the object (output) beam from an electron-impact excitation. For example, a plane-wave object beam propagating at a polar angle of 30° to the surface-normal produces the pattern of offset concentric oval rings shown inset to Fig. 1a. The interference pattern obtained is converted to a binary mask (Fig. 1b) for ease of fabrication by focused ion beam milling on an optically thick (140 nm) polycrystalline gold film (Fig. 1c) deposited by resistive evaporation. It should be noted that the computed holographic (interference) patterns are two-dimensional, that is they provide no information on the required height/depth of surface-relief features for optimal coupling efficiency, which will generally depend on the relative efficiencies of SPP and TR generation, emission wavelength and polar angle. In the present case, features are etched to a depth of 60 nm, which is found, both computationally (in simulations of a binary gold surface-relief hologram driven by a dipole source at $h = 50$ nm, constrained to a $10 \times 10 \times 10$ nm $^3$ domain) and experimentally, to maximize 800 nm emission intensity at $\theta = 30^\circ$.

**Directional plane-wave emission.** Electron-incident radiation emission spectroscopy and imaging have emerged in recent years as powerful tools, variously with nanometre spatial and picosecond temporal resolution, for the characterization of plasmonic modes, crystallographic defects, carrier dynamics, luminescence lifetimes and the local density of optical states in photonic and optoelectronic nanostructures. In the present case, the spectral and directional distribution of electron-induced light emission from holographic structures is characterized in a scanning electron microscope operating in fixed-spot mode, with an electron energy of 30 keV and beam diameter of 50 nm. Emitted light is collected by a parabolic mirror located above the sample and directed to either a VIS/NIR spectrometer or a CCD camera configured to image the parabolic mirror surface, that is to map the angular distribution of light emission (Fig. 2a).

Figures 2b,c present the 800 ± 20 nm light emission distributions for electron injection, at a beam current of 12 nA, respectively on the unstructured gold surface and at the centre of the holographic nanostructure shown in Fig. 1c. The asymmetry seen in the broadly divergent transition radiation pattern from the unstructured surface—Fig. 2b—is an instrumental artefact related to mirror alignment imperfection and does not depend on sample rotation or polycrystalline domain orientation. In stark contrast to the flat gold surface, the holographic nanostructure produces strongly directional emission at $\theta = 30^\circ$, as per design (Fig. 2c) with a peak emission intensity in the selected direction that is increased by around two orders of magnitude.

The holographic nanostructure is essentially a diffractive element, which implies that it should exhibit a dispersive response for light emission at wavelengths other than the design wavelength. This is illustrated in Fig. 3a, where emission intensity integrated over all azimuthal angles is plotted as a function of polar angle for emission wavelengths, 600, 700, 800 and 900 ± 20 nm. Shorter/larger wavelengths are directed at smaller/larger polar angles respectively, with peak emission intensity falling on either side of the structural design wavelength ($\theta = 30^\circ$ the azimuthal angle being arbitrarily set by in-plane sample rotation beneath the incident electron beam; signals are integrated over a 20 s sampling period).
Figure 3 | Performance of gold surface holographic light sources. (a) Emission intensity as a function of polar angle \( \theta \) (integrated over all azimuthal angles) in 40 nm wavelength bands centred at 600, 700, 800 and 900 nm, for a 30 \( \mu \)m \( \times \) 30 \( \mu \)m pattern engineered for 800 nm emission at \( \theta = 30^\circ \) (electron beam current = 6.1–6.3 nA; integration time = 30 s). (b) Peak intensity and 3 dB full-width half-maximum spot size of 800 \pm 20 nm light emission (evaluated at the brightest pixel and as solid angle around said pixel respectively) as functions of the in-plane dimensions of the holographic structure in microns (beam current = 5.0–5.2 nA; integration time = 30 s; dashed trend lines are exponential curves with a growth/decay constant of 20 \( \mu \)m; Error bars for intensity are evaluated as the difference between the peak pixel intensity and the peak of a Gaussian fit to the polar cross-section through that pixel, and for spot size by including \( \pm 1 \) pixel either side of the 3 dB boundary, weighted for relative brightness, in the evaluation of solid angle). Sections of angular emission intensity distributions are shown inset for holograms with centre-edge distances of 5, 15 and 25 \( \mu \)m (polar and azimuthal grids are in 15\(^\circ\) and 30\(^\circ\) steps respectively).

Vortex beam generation. The holographic design approach can readily be applied to generate more complex wavefronts than the plane-wave considered thus far. To illustrate this, we fabricated holographic nanostructures encoded with optical vortex beams\(^{36}\). Such beams have a phase that varies in a corkscrew-like manner along the direction of propagation, described by azimuthal phase dependence \( e^{i\phi} \), where \( \phi \) is the azimuthal angle with respect to the beam axis and \( l \) is an integer known as the topological charge (\( l = 0 \) representing a plane wavefront). They are non-diffracting, have a characteristic ring-shaped intensity profile and carry orbital angular momentum that can be transferred to illuminated objects, making them particularly interesting for optical trap and tweezers applications\(^{37,38}\). Holographic structures were designed to generate optical vortex beams of varying topological charge, again at a polar angle \( \theta = 30^\circ \) and a wavelength of 800 nm, for an electron energy of 30 keV. These comprise patterns of interlocking spiral arms, with the number of arms corresponding to the topological charge, as illustrated in Fig. 4a for \( l = 3, 6 \) and 9. Fig. 4b shows the far-field distribution of the light emitted from holographic nanostructures of \( l = 3, 6 \) and 9 respectively. The observed ring-shaped intensity profile, with a
central intensity null arising as a consequence of the phase singularity on the beam axis, is a defining characteristic of vortex beams. The expected increase in ring radius with topological charge, as \( \sim |l|^{-1/2} \) (analytically derived in ref. 39), is very clearly seen in Fig. 4c.

**Discussion**

In summary, we have shown experimentally that holographically nanostructured surfaces can be employed to control the waveform of light emission from nanoscale sources. The concept is demonstrated in application to the transition radiation and surface plasmon polaritons generated by electron beam impact on a metal (gold) surface, with holographic patterns engineered to produce directed, low-divergence, directional plane wave and optical vortex beams. Brightness (evaluated in photons per unit solid angle per electron) at the design wavelength is enhanced by as much as two orders of magnitude in the present case, and stronger enhancement may be achieved at shorter wavelengths where electron-induced excitation of SPPs is more efficient.

The control of energy transfer and conversion, in particular the generation of light, in nanoscale systems is a technological challenge of great and growing importance. With micron-scale dimensions and the freedom to fully control radiation parameters, holographic free-electron light sources offer novel applications in such areas as nano-spectroscopy, nano-chemistry and sensing. With an appropriate reference field model, the approach can be adapted to a variety of nanoscale 'point source' emitters, for example quantum dots and fluorescent molecules, to other substrate media, and to higher electron energy domains.

The use of continuously-variable-depth, as opposed to binary, holographic nanostructures and phase-gradient metasurface patterns\(^{40}\) may add additional degrees of freedom to the control of emission spectrum/wavefront and device efficiency without the complications of multilayer device architectures.

**Methods**

**Numerical simulation of electron-induced fields.** For the purposes of designing holographic surface structures, the distribution of electromagnetic field in the gold/vacuum interface plane resulting from free-electron injection are computed using the model of a fixed dipole above the surface\(^{21–24}\), via the finite element method (in COMSOL Multiphysics). We select a surface-dipole separation \( h = 50 \text{ nm} \) \((2/16)\) that is small enough to correctly reproduce the electron-induced fields (there is negligible variation in the transition radiation distribution among values of \( h < 1/8 \), that is \(< 100 \text{ nm in the present case})\) whilst being larger than the local finite element mesh size \(20 \text{ nm})\, so as to avoid anomalies in simulated electromagnetic field distributions. The gold and vacuum are assumed to be semi-infinite in the \( z\)-direction, with material parameters for gold taken from ref. 41.

**Electron-induced light emission mapping.** Light emitted as a consequence of electron interaction with samples is collected by a parabolic mirror located above the sample, so as to be confocal with the incident electron beam (which passes through a small hole in the mirror), and directed to either a VIS/NIR spectrometer (Horiba HR320 imaging spectrometer with nitrogen-cooled detector array) or a CCD camera configured to image the parabolic mirror surface, that is to map the angular distribution of light emission. Band-pass filters may be optionally inserted in the latter, imaging beam path. In this work we present as-recorded angle-resolved emission data for all samples, converted directly from the square CCD array to spherical coordinates without background subtraction or post-processing correction for instrumental asymmetry (the \( x/y/z \) position of the mirror is routinely adjusted to correctly centre and frame the CCD emission map image, but no tilt/tilt adjustment is available for fine-tuning) – the need of which is negated by the brightness and directivity of holographic sample emission. The self-consistency of data sets (such as in Figs 3 and 4) against instrumental alignment artefacts is ensured through the use of fixed azimuthal and/or polar angles in each case.

**Data Availability** The data from this paper can be obtained from the University of Southampton ePrints research repository, DOI: 10.5258/SOTON/383663.

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Acknowledgements

This work was supported by the Engineering and Physical Sciences Research Council, UK (Project EP/G060363/1). N.I.Z further acknowledges the support of the Singapore Ministry of Education (grant MOE2011-T3-1-005); and G.L. that of the China Scholarship Council and Longwen Scholarship (State Key Program for Basic Research of China, grant YJK2110D0N0), as well as Prof. Xiaoshuang Chen and Wei Lu (Shanghai Institute of Technical Physics).

Author contributions

J.-K.S. conceived the idea; J.-K.S., K.F.M. and N.I.Z. planned the experiments; B.P.C. fabricated holographic nanostructures and developed the angle-resolved electron-induced light emission measurement systems; G.L. and B.P.C. conducted numerical simulations and performed experimental measurements on holographic nanostructures; B.P.C. fabricated holographic nanostructures and developed the angle-resolved electron-induced light emission measurement systems; All authors contributed to the analysis and interpretation of results; J.-K.S. and K.F.M. wrote the paper; K.F.M. and N.I.Z. supervised the project.

Additional information

Competing financial interests: The authors declare no competing financial interests.

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How to cite this article: Li, G. et al. Holographic free-electron light source. Nat. Commun. 7, 13705 doi: 10.1038/ncomms13705 (2016).

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