Extracting Hα flux from photometric data in the J-PLUS survey

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ABSTRACT

Aims. We present the main steps that will be taken to extract Hα emission flux from Javalambre Photometric Local Universe Survey (J-PLUS) photometric data.

Methods. For galaxies with z < 0.015, the Hα+[N ii] emission is covered by the J-PLUS narrow-band filter F660. We explore three different methods to extract the Hα + [N ii] flux from J-PLUS photometric data: a combination of a broad-band and a narrow-band filter (r′ and F660), two broad-band and a narrow-band filter (r′, i′ and F660), and an SED-fitting based method using eight photometric points. To test these methodologies, we simulated J-PLUS data from a sample of 7511 SDSS spectra with measured Hα flux. Based on the same sample, we derive two empirical relations to correct the derived Hα+[N ii] flux from dust extinction and [N ii] contamination.

Results. We find that the only unbiased method is the SED fitting based method. The combination of two filters underestimates the measurements of the Hα + [N ii] flux by 22%, while the three filters method are underestimated by 9%. We study the error budget of the SED-fitting based method and find that, in addition to the photometric error, our measurements have a systematic uncertainty of 4.3%. Several sources contribute to this uncertainty: the differences between our measurement procedure and that used to derive the spectroscopic values, the use of simple stellar populations as templates, and the intrinsic errors of the spectra, which were not taken into account. Apart from that, the empirical corrections for dust extinction and [N ii] contamination add an extra uncertainty of 14%.

Conclusions. Given the J-PLUS photometric system, the best methodology to extract Hα + [N ii] flux is the SED-fitting based method. Using this method, we are able to recover reliable Hα fluxes for thousands of nearby galaxies in a robust and homogeneous way. Moreover, each stage of the process (emission line flux, dust extinction correction, and [N ii] decontamination) can be decoupled and improved in the future. This method ensures reliable Hα measurements for many studies of galaxy evolution, from the local star formation rate density, to 2D studies in spatially well-resolved galaxies or the study of environmental effects, up to m_r = 21.8 (AB; 3σ detection of Hα+[N ii] emission).

Key words. Galaxies:interactions – Galaxies: statistics

1. Introduction

One of the most important processes driving the evolution of galaxies is the rate at which their gas is transformed into stars, namely the star formation rate (SFR). This parameter accounts for the amount of gas that is transformed into stars per unit time in a galaxy or a region of a galaxy. When the SFR is computed within a given cosmological volume, a SFR density (ρSFR) is obtained.

The most direct indicator of the star-forming process is the ultraviolet (UV) radiation produced in the photosphere of young stars with intermediate to high masses (M ≳ 3M⊙). These stars emit more energy at short wavelengths (λ < 3000Å) than at longer wavelengths. As these stars are massive, their lifetimes are shorter than 300 Myr. Hence, UV traces star formation episodes of these timescales. The UV photons are, however, severely affected by dust extinction, which makes it difficult to translate UV flux into an SFR. Additionally, Earth’s atmosphere blocks most of UV radiation, which makes ground-based surveys in this wavelength range impossible.

The UV radiation field of the most massive O stars (M ≳ 20M⊙) ionize the gas surrounding newborn stars. Hydrogen recombination leads to emission lines in different wavelength ranges, creating the Balmer series, among others. Thus, another widely used SFR indicator is the Hα emission that is originated in the nebular cloud surrounding the star-forming region. This emission is prominent during the first ~ 10 Myr of the star formation process, as the stars that can produce ionising photons die in these timescales. Hence, Hα emission probes more recent bursts than the UV. Moreover, this emission is less affected by dust than the UV continuum. Several calibrations exist to relate Hα emission with the SFR (e.g. Kennicutt [1998] or Calzetti [2013]).

Apart from these, there are other indirect SFR indicators. For example, the infrared (IR) thermal emission of dust heated by the UV field (see, for instance, Calzetti et al. [2007] or Pérez-González et al. [2008], or the forbidden [O iii] λλ3727, 3729 doublet (Kewley et al. [2004], Sobral et al. [2012]). The latter is useful for studies in the optical for objects at z ≥ 0.4, where Hα emission is shifted to the IR.

The SFR has been studied looking at Hα for more than 20 years, both in the local Universe and at higher redshifts. For example, the study of Gallego et al. [1995] computed the SFR density in the local Universe with the UCM Survey data (Zamorano et al. [1994]; Gallego et al. [1995]). The work by Ly et al. [2007] uses narrow-band photometry to derive the luminosity function (LF) and the SFR at 0.07 ≤ z ≤ 1.47 using information of Hα and [O iii]. Finally, the High Redshift Emission Line Survey (HiZELS; Geach et al. [2008]) also studied Hα emission at z = 2.23, 1.47, 0.84 and 0.40, using narrow-band
photometry to estimate the SFR evolution of the last ~ 11 Gyr of the Universe (Sobral et al. 2013).

With the Javalambre Photometric Local Universe Survey (J-PLUS)\(^1\) we aim to derive the SFR of the local Universe measuring the H\(_\alpha\) emission of nearby galaxies (\(z \leq 0.015\)). The design and survey strategy of J - PLUS allows us to probe the faint end of the LF(H\(_\alpha\)). It is expected to reach \(~ 10^{39}\) erg \(\cdot\) s\(^{-1}\), which is 2.5 orders of magnitude deeper than the UCM Survey and the KPNO International Spectroscopic Survey (KISS, Salzer et al. 2000, 2001). In addition, thanks to the large surveyed volume, the bright end of the luminosity function is also constrained.

The goal of this paper is to find the best method to extract H\(_\alpha\) fluxes from the J-PLUS photometric data. We present the methodology to analyse J-PLUS spectral energy distributions (SEDs), and the estimation of the errors that arise with this methodology. The paper is organized as follows: Section 2 summarizes the J-PLUS photometric system and the main characteristics of the J – PLUS survey. Section 3 presents the different methodologies that can be used to recover emission line fluxes from photometric data with a combination of broad-band and narrow-band filters, and in concrete the emission of H\(_\alpha\) \([\text{N} \text{II}]\). In Section 4 we test these methodologies with simulated J-PLUS photo-SEDs, based on a sample of 7511 Sloan Digital Sky Survey (SDSS) spectra of star-forming galaxies with measured H\(_\alpha\) fluxes. In Section 5 we study the errors involved in the methodology. Dust and \([\text{N} \text{II}]\) corrections are treated in Section 6. Finally, in Section 7 we give the most relevant results and conclusions of the work. Throughout this work, magnitudes are given in the AB system (Oke & Gunn 1983).

2. The J-PLUS Survey

The J-PLUS survey is an auxiliary survey of the Javalambre-PAU Astrophysical Survey (J-PAS; Benítez et al. 2014). J-PLUS will be carried out at the Observatorio Astrofísico de Javalambre (OAJ; Cenarro et al. 2014) using the Javalambre Auxiliary Survey Telescope (JAST/T80) and T80Cam (Marin-Franch et al. 2012). This is a wide-field camera (2.1 deg\(^2\) per exposure) installed at the Cassegrain focus. It is equipped with a 9.2k-by-9.2k CCD with a pixel scale of 0.53" pixel\(^{-1}\).

Expected to start in 2015, J-PLUS will cover an area of \(~ 8500\) deg\(^2\) of the northern sky, and has been particularly designed to carry out the photometric calibration of J-PAS using a specific set of 12 filters: 5 broad-band, and 7 narrow-band filters located at key stellar spectral features. Fig. 1 shows the transmission curves of the filters. This filter set allows us to retrieve accurate SEDs for millions of calibration stars, which will be used to transport the photometric calibration from J-PAS to J-PLUS (Gruel et al. 2012).

In addition to the calibration goals, J-PLUS has been designed to acquire the H\(_\alpha\) flux of the galaxies in the nearby Universe (\(z \leq 0.015\)) using one of the narrow-band filters (F660) up to a detection magnitude \(~ 22.5\) in that band (see Table 1 for details of the J-PLUS photometric system). Moreover, the large field of view and efficiency of JAST/T80 and T80Cam make J-PLUS a powerful survey for other galaxy evolution studies, particularly those that require spatially well-resolved galaxies.

![Image 1](http://www.j-plus.es)

**Fig. 1.** J-PLUS photometric system. Solid lines are the theoretical transmission curves of the broad-band J-PLUS filters. Coloured areas denote the theoretical transmission curves of the narrow-band J-PLUS filters. The dashed line represents the quantum efficiency of the T80Cam.

3. Methodologies

In this section, we present a collection of methods that can be used to obtain the flux of H\(_\alpha\) \([\text{N} \text{II}]\) using J-PLUS photometric data. The width \((\sim 150\AA)\) and central wavelength \((6600 \AA)\) of F660 filter ensures that we enclose the three lines inside the filter at \(z \leq 0.015\). We present the basic assumptions of each method and the most relevant equations in the following sections.

3.1. Two filters (2F) method

The simplest method that can be used is a combination of two filters: one to trace the continuum, and another to contrast the emission line. This can be achieved with either two adjacent or overlapping filters. Given the J-PLUS filter system, we test the case that involves a broad filter to trace the continuum (\(r'\)), and a narrow filter placed at the wavelength range of the line of interest (F660). This methodology is widely used in many photometric studies (e.g. Ly et al. 2007; Takahashi et al. 2007; Villar et al. 2008; Koyama et al. 2014; An et al. 2014); see also the studies of the H\(_\alpha\) galaxy survey (James et al. 2004) for a combination of non-overlapping narrow-band filters.

In this case, and taking into account that \(r'\) contains the flux of the H\(_\alpha\) \([\text{N} \text{II}]\) lines, the flux of these emissions can be recovered following the standard recipe (see Pasquali et al. 2007 for a detailed description):

\[
F_{H\alpha+[\text{N} \text{II}]} = \Delta F_{660} \frac{\bar{F}_{660} - \bar{F}_{r'}}{1 - \frac{\bar{F}_{660}}{\bar{F}_{r'}}},
\]

where \(\bar{F}_{660}\) and \(\bar{F}_{r'}\) are the observed average fluxes inside the F660 and \(r'\) filters, and \(\Delta S\) is defined for any passband \(x\) at any wavelength of interest \(\lambda_s\) as

\[
\Delta S = \int P_x(\lambda) \lambda d\lambda.
\]

where \(P_x\) is the transmission of the passband \(x\) as a function of wavelength. In our case, \(\Delta S = \lambda_{H\alpha}\) at \(z = 0\), i.e. \(\lambda_s = 6562.8 \AA\). For J-PLUS F660 and \(r'\) filters, we found \(\Delta F_{660} = 125.3 \AA\) and

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\(^1\) \text{http://www.j-plus.es}
\[ \Delta \nu = 1419 \text{ Å}. \] The strongest assumption of this approximation is a flat continuum inside the \( r' \) filter.

### 3.2. Three filters (3F) method

To solve the problem of the flat continuum assumption of the 2F method, we can use two filters to trace a linear continuum, and a narrow-band filter to contrast the line. There are different configurations for this method: in the work by [Kennicutt & Kent (1983)](https://doi.org/10.1086/159655) no overlapping between the three filters occurs, while the case of the narrow-band filter overlapping two broad filters is studied in [Pascual et al. (2007)](https://doi.org/10.1051/0004-6361:20065456).

Because of the filter configuration of J-PLUS, we test the case in which the continuum is inferred using \( r' \) and \( i' \), while the emission is inside \( F660 \). As in the 2F method, the \( r' \) flux also contains the lines’ flux, and it is risen from the stellar continuum. Because of this, we use an analytic formula to remove the H\(_\alpha + [\text{N} \text{II}] \) contribution inside the \( r' \) filter, i.e.

\[
F_{\text{H} \alpha + [\text{N} \text{II}]} = \frac{(\overline{F}_{r'} - \overline{F}_{i'}) - (\frac{\alpha_{r'} - \alpha_{i'}}{\alpha_{r'} - \alpha_{i'}})(\overline{F}_{660} - \overline{F}_{i'})}{\beta_{660}(\frac{\alpha_{\text{H} \alpha + [\text{N} \text{II}]} - \alpha_{i'}}{\alpha_{r'} - \alpha_{i'}}) + \beta_{r'}},
\]

where \( \overline{F} \) are the observed average fluxes, and \( \alpha \) and \( \beta \) are defined as

\[
\alpha_x \equiv \frac{\int \lambda^2 P_x(\lambda) \, d\lambda}{\int P_x(\lambda) \, d\lambda}, \quad \beta_x \equiv \frac{\lambda_x P_x(\lambda = \lambda_x)}{\int P_x(\lambda) \, d\lambda},
\]

where in our particular case, \( \lambda_x = \lambda_{\text{H} \alpha} = 6562.8 \text{ Å} \). These equations are detailed in the Appendix A.

### 3.3. SED-fitting method

This method benefits from all the J-PLUS filters to infer the emission flux after fitting the stellar continuum of the galaxy. To do that, we compare simulated J-PLUS observations with a set of template models, and for each pair observation-template, we compute the value of the \( \chi^2 \) function, defined as

\[
\chi^2 = \sum \left( \frac{\overline{F}_x - k_j \overline{T}_j}{\delta_x} \right)^2,
\]

where \( \overline{F}_x \) is the observed flux for each of the \( x \) filter with its error \( \delta_x \), \( \overline{T}_j \) is the flux inside the \( x \) filter of the \( j \) template, and \( k \) scales the templates at the magnitude of the galaxy that we are fitting. We estimate this scaling parameter for each \( j \) template by minimizing Eq. 5, i.e.

\[
k_j = \frac{\sum_i \left( \frac{\overline{F}_x}{\delta_x} \right)}{\sum_i \left( \frac{\overline{T}_j}{\delta_x} \right)},
\]

Model templates are simple stellar populations (SSPs) taken from [Bruzual & Charlot (2003)](https://doi.org/10.1051/0004-6361:20030906) (BC03 hereafter), with 40 ages from 1 Myr to 13.75 Gyr in logarithmic bins, a [Salpeter (1955)](https://doi.org/10.1007/BF01621834) initial mass function, and six metallicities ranging from 0.2Z$_\odot$ to 2.5Z$_\odot$. We extinguish these models with a [Calzetti et al. (2000)](https://doi.org/10.1086/317387) law from \( E(B-V) = 0 \) to \( E(B-V) = 1 \) in steps of 0.05. In the end we have 4000 templates at rest-frame. These are convolved with the J-PLUS photometric system properties using PySynphot. The template fluxes are then

\[
\overline{T}_j = \frac{\int T_j P_x(\lambda) \, d\lambda}{\int P_x(\lambda) \, d\lambda}.
\]

The \( \chi^2 \) fitting is carried out without taking the flux of the \( F660 \) filter into account, which contains the H\(_\alpha + [\text{N} \text{II}] \) emission fluxes. To derive the emission flux, we approximate it as a single line described as a Dirac’s delta function. This is called “the infinite thin line approximation” (see, for instance [Pascual et al. (2007)](https://doi.org/10.1051/0004-6361:20065456)). If we split the total \( F660 \) flux into two components (continuum and emission) and introduce it into Eq. 7, we get

\[
\overline{F}_{660} = \frac{\int \left( F_{\text{H} \alpha + [\text{N} \text{II}]} + F_{\text{cont}} \right) P_{660}(\lambda) \, d\lambda}{\int P_{660}(\lambda) \, d\lambda},
\]

where \( F_{\text{H} \alpha + [\text{N} \text{II}]} \) is the emission flux, and \( F_{\text{cont}} \) the continuum. If we assume that \( F_{\text{H} \alpha + [\text{N} \text{II}]} = F_{\text{H} \alpha + [\text{N} \text{II}]} \delta(\lambda - \lambda_{\text{H} \alpha}) \), and split Eq. 6 in two integrals, we get

\[
\overline{F}_{660} = \overline{F}_{660, \text{cont}} + \frac{1}{\Delta F_{660}} F_{\text{H} \alpha + [\text{N} \text{II}]}.
\]

Table 1. J-PLUS photometric system properties.

| Filter name | Central wavelength (nm) | FWHM (nm) | mag (AB) S/N=3 | mag (AB) S/N=50 | Comments |
|-------------|------------------------|-----------|----------------|----------------|----------|
| u'          | 348.5                  | 50.8      | 23.00          | 19.69          | In common with J-PAS |
| F378        | 378.5                  | 16.8      | 21.58          | 18.01          | [O iii]; in common with J-PAS |
| F395        | 395.0                  | 10.0      | 21.60          | 18.01          | Ca H+K |
| F410        | 410.0                  | 20.0      | 21.62          | 18.03          | Hδ |
| F430        | 430.0                  | 20.0      | 21.65          | 18.01          | G-band |
| g'          | 480.3                  | 140.9     | 23.23          | 19.92          | SDSS |
| F515        | 515.0                  | 20.0      | 21.67          | 18.01          | Mg |
| r'          | 625.4                  | 138.8     | 23.26          | 19.99          | SDSS |
| F660        | 660.0                  | 13.8      | 22.64          | 19.11          | Hα+[N ii]; in common with J-PAS |
| r'          | 766.8                  | 153.5     | 22.31          | 18.88          | SDSS |
| F861        | 861.0                  | 40.0      | 21.48          | 18.01          | Ca Triplet |
| z'          | 911.4                  | 140.9     | 21.51          | 18.19          | SDSS |

\(^{2}\) A Python programming language adaptation of the widely used Synphot, developed by the Space Telescope Science Institute (STSCI)}
with the 3F method. In order to obtain a more reliable result, we perform 500 Monte Carlo runs. To do that, we keep the 3F methodology.

3.4. Measurements and error estimation

We present an example of an SED fitting in Fig. 2, and compare the continuum that results from the equations of the 2F and 3F methodologies.

3.4. Measurements and error estimation

To test each methodology, we use a set of SDSS spectra with emission lines measured by the Portsmouth Group (Thomas et al. 2013) in the 10th Data Release (DR10). We excluded Barion Oscillation Spectroscopic Survey (BOSS, Dawson et al. 2013) galaxies, as its targets are luminous red galaxies at $z \geq 0.2$. We selected all the objects that were classified as star forming by the Portsmouth group, according to a BPT diagram criteria (Baldwin et al. 1981). Thus, we do not expect a significant AGN contamination in the sample. We applied a spectroscopic redshift cut at $z < 0.02$. This redshift cut is chosen to probe a volume big enough to have a large number of galaxies with similar properties as the expected J-PLUS sources. After applying these criteria, we are left with $\sim 12000$ spectra.

From this sample, we retain only the spectra with a Hα equivalent width (EW<sub>Hα</sub>) $12 \lesssim \mathrm{EW}_{\mathrm{H}\alpha}$. This cut was done assuming that J-PLUS cannot resolve, with a precision of 3σ, EW<sub>F660</sub> $\lesssim 12 \mathrm{\AA}$ because of the errors in the determination of magnitude of the zero point. From [Pascual et al. (2007)] we know that

$$\mathrm{EW} = \Delta_{660}(Q - 1) \frac{Q - 1}{1 - Q\epsilon},$$

where $\epsilon \equiv \lambda_{\mathrm{rest}}/\lambda_r$, and $2.5 \log Q = m_r - m_{F660}$. Assuming a systematic error in the determination of the zero-point magnitude of $\delta m \approx 0.02$ in $r'$ and F660, there is a limiting difference in magnitudes of $\delta m \sim 0.03$, which we cannot resolve with enough confidence, and which leads to a minimum EW of detection that is $\mathrm{EW}_{F660} \approx 12 \mathrm{\AA}$. From the SDSS data we cannot know the observed EW<sub>F660</sub>, so we take $\mathrm{EW}_{\mathrm{H}\alpha} = 12 \mathrm{\AA}$ as lower limit. Finally, a last cut in the median signal-to-noise ratio (S/N) of each spectrum was done. Only spectra with average S/N $\geq 5$ are kept. This limit is chosen to guarantee that spectroscopic flux errors are not important.

After applying these criteria, the sample contains 7511 spectra. We refer to this sample as S1. Figure 2 presents the distribution of the S1 as a function of the EW<sub>F660</sub> and $m_r$. As, for now, the redshift is not taken into account in our analysis, we shifted all the spectra of S1 to $z = 0$. After this, we convolved them with the J-PLUS filters that are in the wavelength range of the SDSS spectra to obtain $F_{\lambda}$. Because these spectra have a shorter wavelength range than J-PLUS filters, we lose the information of $\lambda_{ij}$, $F_{337}$, and $z$ bands. The convolution retrieves the apparent magnitudes and mean fluxes of each passband. We stress that these apparent magnitudes are computed from the flux enclosed inside the fibre, and are not representative of the whole galaxy. With the apparent magnitudes, we compute the expected S/N using the J-PLUS exposure time calculator. This tool provides the estimated S/N given an apparent magnitude, an exposure time (that can be divided into several exposures) and different sky conditions. The assumed conditions to compute the S/N values were a grey night, a seeing of 0.9 arcsec, a photometric aperture of 1.8 arcsec, and an airmass of 1.2. With this, the flux error in each passband $x$ is $\delta x = \sigma x / \mathrm{S/N}$. We apply each of the methodologies explained in Sect. 3 to the J-PLUS photo-spectra of S1 and study the performance of each methodology below.

4.2. J-PLUS vs. SDSS

At this point we test the precision of each method described in Sect. 3 to recover the flux of Hα + [N ii]. To this aim, we compare our inferred fluxes with those provided by the Portsmouth Group. As their values are dust corrected, but the SDSS spectra
are not, we add dust to the SDSS measurements following the Calzetti et al. (2000) extinction law with $R_V = 4.05$, which the Portsmouth group applied, and the values of the extinction law provided by them.

We apply each methodology to the spectra of S1, and compare the recovered flux of $\mathrm{H}\alpha + [\mathrm{N\,ii}]$ lines with the spectroscopic measurements,

$$R = \frac{\langle F_{\mathrm{H}\alpha + [\mathrm{N\,ii}]} \rangle}{F_{\mathrm{H}\alpha + [\mathrm{N\,ii}]}}. \quad (14)$$

where, in this case, $F_{\mathrm{H}\alpha + [\mathrm{N\,ii}]}^{\mathrm{SDSS}}$ is

$$F_{\mathrm{H}\alpha + [\mathrm{N\,ii}]}^{\mathrm{SDSS}} = [F_{\mathrm{H}\alpha} + F_{[\mathrm{N\,ii]},.6548} + F_{[\mathrm{N\,ii]},.6585}] \times 10^{-1.33 \cdot (B-V)} \quad (15)$$

because we are adding dust attenuation to its measurements. The resulting distribution of ratios $R$ is fitted to a Gaussian in all the cases.

4.2.1. 2F and 3F methods

We show the resulting distribution of $R$ when we analyse the spectra applying the 2F and 3F methodologies in Fig. 4. The 2F method is biased, mostly because we assume a flat continuum that is given by the broad filter. We lose the information about the colour of the galaxy, i.e. the true shape of the continuum at the wavelength range of the emission line. The distribution of results is very asymmetric, and cannot be fitted to a Gaussian distribution. The median of this distribution is $\mu = 0.78$, while the dispersion is given by $\sigma = 0.5 \times (P_{84} - P_{16}) = 0.20$, where $P_{84}$ and $P_{16}$ are the 84th and 16th percentiles, respectively.

To cope with this bias, Sobral et al. (2009, 2012), and subsequent works from the HiZELS survey, and also the work by Ly et al. (2011), introduce a correction based on the broad-band to narrow-band colour. This correction is applied to compensate the flat continuum assumption and the difference between the central wavelength of the broad-band filter and the narrow-band central wavelength. This correction would be a step between the 2F and 3F method. However, we prefer the 3F method, as its correction is analytic.

With the 3F method, the distribution of results becomes almost Gaussian, but a bias of ~ 9% still persists, with $\mu = 0.91$ and a dispersion $\sigma = 0.06$ from the Gaussian fit. In this case, we are more sensitive to the true shape of the continuum in the wavelength range of the line, but we still have to assume it is linear, which is a poor approximation because of the $\mathrm{H}\alpha$ absorption.

4.2.2. SED fitting

We plot the distribution of results after applying the SED fitting methods in Fig. 5. We compare the results without applying the $r'$ decontamination. The SED fitting routine with $r'$ decontamination performs better than the SED independent methodologies (i.e. the 2F and 3F methods), being unbiased ($\mu_{\mathrm{SED}} = 1.00$). With this technique, we do not approximate the continuum to any function; we use the continuum inferred from BC03 templates, which also contain an estimation for the absorption of $\mathrm{H}\alpha$. Another interesting result is the impact that has the $\mathrm{H}\alpha + [\mathrm{N\,ii}]$ emission inside the $r'$ filter. Not taking this into account causes a bias in our results by ~ 8%.
4.3. Testing the methodologies: conclusions

At this point we conclude that the methodologies that only use two or three filters are inconvenient for J-PLUS, given our filter configuration, as they produce biased results in average. In the case of the 2F methodology with no colour correction, this bias is ~ 22%, while the 3F method underestimates the Hα + [N II] flux by 9%. As Sobral et al. (2012) points out, this effect when using only two filters is, in part, caused because the central wavelength of the narrow filter does not coincide with the broad-band central wavelength. To cope with this, we need more information, and so we include the i` filter. However, this does not solve totally the problem.

With the SED fitting procedure we avoid this bias, though attention must be paid to the contribution of Hα + [N II] inside the r′ filter. Not taking this effect into account biases our results by 8%. Finally, the SED fitting procedure with the r′ decontamination is unbiased and has a dispersion of σ_{SED} = 0.06. This dispersion is a combination of the errors associated with the photometry, δ_{phot}, and other factors that are discussed in detail in Sect. 5.4.

5. SED fitting routine: performance and error budget

In the previous section, we conclude that the SED fitting routine is the most reliable methodology for our purposes given the J-PLUS filter configuration. In this section, we perform some additional tests on this methodology and explore the error budget in the measurements.

5.1. Dependence on m_{r′}

To see if any bias appears at faint magnitudes, we study the distribution of R at several m_{r′} bins. To do that, we selected the galaxies in S1 within a m_{r′} range and fit a Gaussian to their R distribution. Bins are defined to contain the same number of galaxies, which in this case is 626.

5.2. Dependence on EW

We repeat the same analysis, but binning our S1 as a function of the observed EW_{F660}. This EW is not the one that we used in the data selection criteria, but that resulting from the recovered flux of Hα + [N II].

\[
EW_{F660} = \frac{\langle F_{H\alpha + [N\,II]} \rangle}{F_{660} - \langle F_{H\alpha + [N\,II]} \rangle},
\]

Results are shown in Fig. 7. Each bin contains 375 spectra. In this case, the error weighted median is still unbiased, though the results show a trend in the recovered flux that creates an excess in the region of small EW, and an underestimation in the larger EWs. This latter effect might be due to a bad determination of the continuum in regions dominated by ionized gas, where SSP models are not valid. Nevertheless, the error is constrained to under 4.3%.

5.3. Simulating observations at higher m_{r′}

We have shown that observing at different m_{r′} does not introduce any biases. Our spectroscopic sample however cannot reach the expected J-PLUS m_{r′} limiting magnitude (the selection criteria naturally cut the sample before m_{r′} = 20.5, as seen in Fig. 3). To study the performance of the SED fitting method at magnitudes higher than m_{r′} = 20.5, we have to simulate observations.

5.3.1. Sample S2

We selected a subsample of galaxies with m_{r′} \leq 17.5 and median S/N \geq 20 from the parent sample, which were artificially scaled at any magnitude. These thresholds were chosen to have a subsample of galaxies with good quality data and a reasonable number of spectra to do statistics. In particular, we selected...
5.3.2. Simulation routine

The spectra of S2 are scaled to any \( m_r \) of interest. After we change the magnitude of each filter with the same difference of magnitudes that we apply to match the intrinsic \( m_r \) with the desired \( m_r \), we compute the expected S/N for each filter, and we perturb each of the \( x \) fluxes within its error bar from a random normal distribution with \( \mu = \bar{F}_x \) and \( \sigma = \bar{F}_{i}/\text{S/N}_i \). These perturbed fluxes are now considered the observations, and from these fluxes we estimate \( \langle F_{\text{H}a + [NII]} \rangle \) and its uncertainty following the process described in Sect. 3.4.

Figure 8 shows that we recover the fluxes without biases up to magnitude \( m_r \sim 21.8 \). The errors increase at fainter magnitudes, while remains constrained at \( a \sim 4.3\% \) at brighter magnitudes. We discuss this in the next section.

5.4. Estimating the errors

Here we carry out an analysis of the errors associated with the measurement method. For convenience, we refer to the dispersion of the results, given by the standard deviation of the Gaussian fits, with letter \( \sigma \); we reserve letter \( \delta \) for the errors and uncertainties in the measurements. In Sect. 3.4 we explained how we estimate the photometric errors \( \delta_{\text{phot}} \) of \( \langle F_{\text{H}a + [NII]} \rangle \). However, in Fig. 8 we see that the dispersion of the results in the brightest magnitudes is almost constant. This means that we cannot explain the dispersion of the results only with \( \delta_{\text{phot}} \), and that we need to add a new uncertainty to our measurements, i.e.

\[
\sigma_{\text{SED}} = \sqrt{\sigma^2_{\text{phot}} + \delta^2_{\text{syst}}}. \tag{17}
\]

To compute the value of \( \delta_{\text{syst}} \), we want to minimize \( \delta_{\text{phot}} \). We simulate observations with \( S/N > 10^4 \) for S2. In this case, the dispersion in the results is only due to \( \delta_{\text{syst}} \). Doing this, we find that \( \delta_{\text{syst}} = 0.05 \). The shaded area in Figs. 6, 7 and 8 shows this systematic uncertainty. We see that this value well constrains the error bars until these begin to increase because of photometric errors.

To test the validity of this result, we compare this new error with the purely photometric error. To do that, the Monte Carlo approach described in Sect. 3.4, we create 1134 normal distributions (one per spectrum in S2), centred in \( \mu_1 = 1 \) and with \( \sigma_1 = \delta_{\text{phot}}, \). We see in Fig. 8 that, when we add all these distributions, we recover a new distribution whose dispersion is only due to photometric errors (blue solid line). However, if we repeat the same exercise with \( \sigma_1 = \sqrt{\sigma^2_{\text{phot}} + \delta^2_{\text{syst}}} \), we see that the resulting distribution has a dispersion that resembles that of our results (red dashed line).

Finally, we apply this systematic error to the 7511 spectra of S1. We show in Fig. 10 the same distribution as in Fig. 8, but we overplot the distribution when only taking \( \delta_{\text{phot}} \) (blue solid line) into account and when we add the 4.3\% uncertainty. This new distribution (red solid line) traces the dispersion of our results well, meaning that our error budget is reliable.

5.5. SED fitting routine: performance and error budget conclusions

In this section, we have studied the sources of error that affect our measurements of H\( \alpha + [\text{NII}] \) flux when using the SED fitting method. We have seen that our measurements are not biased at any magnitude of the J-PLUS detection magnitude range. To accomplish this, we studied S1 spectra at their magnitudes and simulated observations of S2 galaxies at magnitudes in which we have no data. With this test, we find that there is an uncertainty in all the magnitudes that is independent of the photometric errors.

We studied this uncertainty and treated it as a source of error. We see that adding a systematic uncertainty of 4.3\% to the \( \delta_{\text{phot}} \) of each measurement, allows us to recover a distribution that reproduces the observed dispersion in the results at any magnitude. This uncertainty can be due to a combination of several sources, such as not taking the intrinsic errors of the SDSS spectra into account, fitting SSPs to regions that may not be well represented by SSPs, or differences in the measurement procedures between our results and the Portsmouth Group.
shows the sum of 1134 normal distributions centred at μ = 1 and σ = σ_{phot}. Red dashed curve is the sum of 1134 normal distributions centred at μ = 1 and with σ = √σ_{phot}^2 + σ_{syst}^2. Bottom panel: same as above, except for spectra scaled to m_V = 21.25.

Fig. 9. Top panel: black histogram denotes the distribution of R for the 1134 galaxies in S2, scaled to m_V = 17.5. Blue curve shows the sum of 1134 normal distributions centred at μ = 1 and with σ = σ_{phot}. Red dashed curve is the sum of 1134 normal distributions centred at μ = 1 and with σ = √σ_{phot}^2 + σ_{syst}^2. Bottom panel: same as above, except for spectra scaled to m_V = 21.25.

Fig. 10. Distribution of R for all the 7511 galaxies in S1. Blue curve denotes the sum of 7511 normal distributions centred at μ = 1 and σ = σ_{phot}. Red dashed curve indicates the sum of 7511 normal distributions centred at μ = 1 and with σ = √σ_{phot}^2 + σ_{syst}^2.

6. Dust correction and [N II] removal

6.1. Dust correction

Our aim is to recover the Hz emission from galaxies; however, galaxies contain dust that is mixed with the stellar populations and gas. Dust is present in molecular clouds before they collapse to form stars, and it is mixed with the hot gas after the first stars of a star-forming region are born. The presence of dust has two important observable consequences: it attenuates the total amount of light that we receive, and tends to redden the true colour of light-emitting region. Both effects have an impact on the absolute and relative fluxes and magnitudes that we measure. Attenuation causes all the magnitudes in the optical and UV to increase, while reddening causes that this increase is higher as we move to the blue parts of the spectrum.

The proportion between the attenuation in the Johnson V band (A_V) and the difference between the observed and the intrinsic (i.e. dust-free) magnitudes of the Johnson B and V bands (i.e. the colour excess E(B − V)) has been called the extinction law (see Cardelli et al. 1989), although definitions in other bands exist (Fitzpatrick 1999), i.e.

\[ R_V = \frac{A_V}{E(B - V)}. \]  

From Calzetti et al. (2000), we know that the relation between the intrinsic flux and the observed one is

\[ F_i(\lambda) = F_o(\lambda)10^{0.4A_V} = F_o(\lambda)10^{0.4E(B-V)k'(\lambda)} \]  

where k'(\lambda) is a polynomial that depends on \lambda and R_V.

To compare the recovered flux with the one provided by the Portsmouth Group, we added dust to their measurements with the values of E(B − V) that they provided (see Eq. 15). However, with the filter configuration of J-PLUS it is more difficult to estimate the dust contribution to our fluxes.

From now on we will be using the SED fitting procedure to extract the flux of Hz + [N II], as the other methodologies presented biases. We stress that the corrections presented in this section can be modified in the future because they are independent of the method that we used to isolate the emission lines.

A common assumption that is applied to photometric data is an attenuation of A_Hα = 1 mag for the Hz emission (see Kennicutt 1992, Geach et al. 2008, Villar et al. 2008, Sobral et al. 2012). The dust-corrected values assuming this attenuation law (see Cardelli et al. 1989, although definitions in other bands exist (Fitzpatrick 1999), i.e.

\[ A_V = E(B - V). \]  

with S1 we find that there is a trend between the observed g′ − i′ colour and the spectroscopically measured E(B − V). This is represented in Fig. 11. To fit a power-law function to these points, we bin this sample in g′ − i′ logarithmically spaced bins and compute the median of each bin. We see in Fig. 11 that, for g′ − i′ ≤ 0.5, medians of E(B − V) are 0. This is because there is a subsample of data, which has E(B − V) = 0 and no associated error. We take them into account as zero for the fit and we obtain...
We avoid negative colour excess values by making $E(B - V) = 0$ if the inferred value is negative. The derived relation should only be used in certain circumstances. The $g' - i'$ colour that we are using here is obtained after convolving the SDSS spectra with the J-PLUS photometric system. This means that this colour is a local property of the region inside the SDSS fibre. With J-PLUS we will have spatially resolved galaxies, where we will be able to differentiate and isolate star-forming regions. These are the regions where this relation is reliable. For galaxies that are not spatially resolved, the $g' - i'$ colour is an overall colour resulting of the underlying stellar populations and the gas, if any. In these cases, the validity of this correction is not ensured, and other SED-fitting codes which study galaxy properties and stellar populations in more detail, may be used to explore dust extinction (see, for instance, MUFFIT, Diaz-Garcia et al. 2015).

### 6.2. $\text{[NII]}$ correction

The $F660$ filter contains the flux of Hα and [NII] doublet, and it is not possible to deblend these three lines to isolate the Hα emission flux. To cope with this problem, empirical relations must be applied. With data from S1, we find that there is a relation between the flux of Hα + [NII] and the Hα flux alone. Figure 13 shows this relation. We find that there is a slight bimodality in the distribution of fluxes, which is blurred in the low-emission regime. This bi-modality can be disentangled with the help of the colour $g' - i'$, and we fit the following equation to each branch:

$$\log(\text{H}α) = \begin{cases} 0.989 \log(F_{\text{Hα}+[\text{NII}]} \text{D.C.)} - 0.193, & \text{if } g' - i' \leq 0.5, \\ 0.954 \log(F_{\text{Hα}+[\text{NII}]} \text{D.C.)} - 0.753, & \text{if } g' - i' > 0.5, \end{cases}$$

where $F_{\text{Hα}+[\text{NII}]} \text{D.C.}$ refers to the $F660$ flux after dust correction.

### 6.3. Hα only measurements

We apply both corrections to our measurements and compare the recovered results with the spectroscopic values of Hα + [NII] without dust and Hα only. As we can see in Fig. 13 both corrections help us to recover the Hα flux without adding any extra bias to the whole set of measurements. To these results, we fit a Gaussian distribution.

It is important to stress that [NII] correction is empirical, and can only be applied after correcting for dust the observed $F660$ flux. This relation should hold regardless of the dust correction that is applied, as it has been calibrated with dust-free data.

### 6.4. Error budget

After correcting the flux of Hα + [NII] from dust, the resulting distribution has a larger dispersion, although it does not become biased. This increase in the dispersion must be taken as another source of uncertainty, namely $δ_{\text{corr}}$, i.e.

$$δ_{\text{Hα}} = \sqrt{δ_{\text{phot}}^2 + δ_{\text{syst}}^2 + δ_{\text{corr}}^2}.$$ (22)

To derive the value of $δ_{\text{corr}}$, we compare the dispersion in distribution of raw Hα + [NII] ($σ_{\text{SED}} = 0.06$, Fig. 5), only with the dispersion of the distribution of Hα ($σ_{\text{Hα}} = 0.15$, Fig. 13). We find that $δ_{\text{corr}} = 0.14$. 

---

**Fig. 11.** Distribution of spectroscopically derived $E(B - V)$ and observed $g' - i'$. Blue dots denote the medians of $E(B - V)$ values enclosed in the logarithmically spaced bins. Red dashed line shows the fit to the blue dots.

**Fig. 12.** Relation between the spectroscopically measured and dust corrected Hα flux and the total Hα + [NII] flux. We see that the distribution is bimodal. The two trends can be differentiated if we split the sample by its observed $g' - i'$ colour.

**Fig. 13.** The empty red histogram is distribution of the recovered Hα + [NII] after correcting for dust; dashed blue histogram denotes the distribution of the recovered Hα flux after correcting for dust and [NII]; Solid lines indicate Gaussian fits to the data. Best-fitting values are labelled in the panel.
Fig. 14. The Histogram is the distribution of the recovered Hα flux after correcting for dust and [N ii]; The solid curve shows the distribution only when taking δphot into account; the dashed curve shows the distribution when adding δsyst and δcorr to δphot.

Combining both uncertainties δsyst (Sect. 5.4) and δcorr, we obtain that the final error in Hα is

$$\delta_{H\alpha} = \sqrt{\delta_{phot}^2 + 0.15^2}. \quad (23)$$

We now add this error to each measurement of S1 spectra and repeat the same analysis as in Sect. 5.4. The resulting distribution, with the fitting properties and the errors, is shown in Fig. 14. We see that a 15% uncertainty creates a distribution that resembles the dispersion of R after correcting for dust and [N ii], as desired.

### 6.5. Dust correction and [N ii] removal: conclusions

In this section, we have studied how to correct for dust extinction and for the contribution of the [N ii] doublet to the total observed flux inside F660. We used two empirical relations derived from SDSS data. Taking the properties of galaxies used to derive these expressions into account, they should be representative of the properties of star-forming regions of galaxies in the local Universe.

When applied, both corrections retrieve unbiased results. This means that we can decouple them from our first goal: obtaining reliable measurements of Hα + [N ii]. In this sense, both corrections can be modified in the future if better corrections are found.

When we add both corrections to the raw measurement of Hα + [N ii], the distribution of results is unbiased, but the dispersion increases. We obtain that the uncertainty introduced when we apply our corrections is δcorr ~ 14%.

### 7. Summary and conclusions

We have presented the capabilities of the J-PLUS survey to infer Hα emission from photometric data. We first presented different methodologies and equations that can be applied to extract emission line fluxes from narrow-band and broad-band photometry. After that, we tested each methodology simulating observations of SDSS spectra as seen by J-PLUS. We find that:

1. Using a broad- and a narrow-band filter without taking care of the colour of the galaxy retrieves severely biased results, tending to underestimate the Hα + [N ii] flux of star-forming galaxies by ~ 20%. The asymmetry of the distribution makes it difficult to treat it statistically and to have the errors under control. To use this methodology, colour corrections should be applied, as shown by Sobral et al. (2009).
2. Using a combination of two broad-band filters and a narrow-band gives better results. However the method is still biased in average by a 9%.
3. Fitting the whole SED to a collection of SSP models after subtracting the Hα + [N ii] flux from r’, retrieves unbiased Hα + [N ii] fluxes. We stress the importance of taking into account the contribution of the emission lines inside the r’ filter. Not correcting the flux of this filter introduces a bias of 8%.

We conclude that the SED fitting method is the best one given the J-PLUS capabilities. We encourage other photometric surveys targeting emission lines with narrow-band filters to explore the SED fitting methodology, instead of restricting them to the use of two or three filters.

To correct the observed Hα + [N ii] emission flux from dust and remove the [N ii] contribution, we derived empirical corrections from the SDSS data. After that, the recovered Hα flux is still unbiased, but suffers a larger dispersion.

Finally, we demonstrate that the error of our measurements of Hα flux, δHα, has three contributions. The first is given by the photometric errors of our data, δphot. The second contribution has several sources, which include not considering the intrinsic errors of SDSS spectra, the use of SSPs to fit the stellar continuum of regions that may not resemble SSPs, and differences between our measurement procedure and the Portsmouth group’s method. This results in a systematic uncertainty, δsyst. The last source of uncertainty is related with the corrections of dust and [N ii], namely δcorr. In the end, we express the error of our Hα measurements as

$$\delta_{H\alpha} = \sqrt{\delta_{phot}^2 + \delta_{syst}^2 + \delta_{corr}^2}. \quad (24)$$

where δsyst = 0.05 (Sect. 5.4) and δcorr = 0.14 (Sect. 6.4). This means that our Hα measurements have a 15% of uncertainty, regardless of the quality of the data.

We stress here that this 15% is an upper limit to the uncertainty related to the methodology and the corrections. Because each stage of the process (emission detection, dust correction, and [N ii] correction) is unbiased, we can decouple them. This would allow us to improve these corrections and reduce the systematic error. For instance, J-PLUS has a narrow filter in the [O ii] wavelength range. This forbidden emission is also a tracer of the SFR, and could help us constrain the dust contribution better than the colour that we used.

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Appendix A: 3F method: Equations

Here we develop the equations for the 3F method that was described in Sect. 3.2. The average flux $\bar{F}_x$ integrated any filter $x$ can be obtained, if the passband $P$ properties are known, with the following expression:

$$\bar{F}_x = \frac{\int F_x P_x (\lambda) \lambda d\lambda}{\int P_x (\lambda) \lambda d\lambda}. \quad (A.1)$$

where $P_x$ is the transmission of the passband $x$, as a function of wavelength.

Inside the $r'$ filter, there are two main contributions: the flux of the continuum $F_{r', \text{cont}}$ and the flux of $H\alpha + [N\text{II}]$, $F_{r', H\alpha+[N\text{II}]}$. Following the same reasoning, in the $F660$ filter is $F_{F660, \text{cont}}$ and $F_{F660, H\alpha+[N\text{II}]}$.

We approximate the continuum to a linear function

$$F_{\text{cont}} (\lambda) = M\lambda + N, \quad (A.2)$$

and for the emission, we assume that the flux of the three lines can be understood as one single, infinitely thin line centred at the $H\alpha$ wavelength, which is described as a Dirac’s delta function (the so-called infinite thin line approximation):

$$F_{\text{line}} \equiv F_{H\alpha+[N\text{II}]} \delta (\lambda - \lambda_{H\alpha}). \quad (A.3)$$

With this, the observed flux inside $r'$:

$$\bar{F}_{r'} = \frac{\int (M\lambda + N) P_{r'} (\lambda) \lambda d\lambda}{\int P_{r'} (\lambda) \lambda d\lambda} + \frac{\int F_{\text{line}} P_{r'} (\lambda) \lambda d\lambda}{\int P_{r'} (\lambda) \lambda d\lambda}. \quad (A.4)$$

Plugging Eqs. (A.2) and (A.3) into Eq. (A.4) and rewriting the integrals, we get

$$\bar{F}_{r'} = \frac{\int (M\lambda + N) P_{r'} (\lambda) \lambda d\lambda}{\int P_{r'} (\lambda) \lambda d\lambda} + \beta_{r'} F_{\text{line}} = M\alpha_{r'} + \beta_{r'} F_{\text{line}} + N, \quad (A.5)$$

where $\alpha$ and $\beta$ can be defined at any passband $x$, at any wavelength of interest $\lambda_x$, as

$$\alpha_x \equiv \frac{\int \lambda^2 P_x (\lambda) \lambda d\lambda}{\int P_x (\lambda) \lambda d\lambda} \quad \beta_x \equiv \frac{\int \lambda P_x (\lambda - \lambda_x) \lambda d\lambda}{\int P_x (\lambda) \lambda d\lambda}. \quad (A.6)$$

In our case, $\lambda_x = \lambda_{H\alpha}$. Following the same steps for the $F660$ and the $i'$ filters, we obtain

$$\bar{F}_{F660} = M\alpha_{F660} + \beta_{F660} F_{\text{line}} + N, \quad (A.7)$$

$$\bar{F}_{i'} = M\alpha_{i'} + N. \quad (A.8)$$

In Eq. (A.8) the line contribution does not appear because the $i'$ filter does not cover it. Combining Eqs. (A.7) and (A.8) we obtain

$$M = \frac{\bar{F}_{F660} - \bar{F}_{i'}}{\alpha_{F660} - \alpha_{i'}}. \quad (A.9)$$

Plugging this into Eq. (A.8)

$$N = \bar{F}_{i'} - \alpha_{i'} \left( \frac{\bar{F}_{F660} - \bar{F}_{i'} - \beta_{F660} F_{\text{line}}}{\alpha_{F660} - \alpha_{i'}} \right). \quad (A.10)$$

With both parameters determined as a function of known values, we can go back to Eq. (A.5) to obtain

$$F_{H\alpha+[N\text{II}]} = \left( \bar{F}_{r'} - \bar{F}_{i'} \right) \left( \frac{(\alpha_{r'} - \alpha_{i'})}{\alpha_{F660} - \alpha_{i'}} \right) \left( \bar{F}_{F660} - \bar{F}_{i'} \right) \left( \frac{\beta_{F660}}{\alpha_{F660} - \alpha_{i'}} \right) + \beta_{r'},$$

which is Eq. (3) from Sect. 3.2.