Low frequency gravitational wave detection with ground-based atom interferometer arrays

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We propose a new detection strategy for gravitational waves (GWs) below a few hertz based on a correlated array of atom interferometers (AIs). Our proposal allows us to reduce the Newtonian noise (NN), which limits all ground based GW detectors below a few hertz, including previous atom interferometry-based concepts. Using an array of long baseline AI gradiometers yields several estimations of the NN, whose effect can thus be reduced via statistical averaging. Considering the km baseline of current optical detectors, a NN rejection of a factor of 2 could be achieved and tested with existing AI array geometries. Exploiting the correlation properties of the gravity acceleration noise, we show that a tenfold or more NN rejection is possible with a dedicated configuration. Considering a conservative NN model and the current developments in cold atom technology, we show that strain sensitivities below $1 \times 10^{-19}/\sqrt{\text{Hz}}$ in the $0.3–3$ Hz frequency band can be within reach, with a peak sensitivity of $3 \times 10^{-23}/\sqrt{\text{Hz}}$ at 2 Hz. Our proposed configuration could extend the observation window of current detectors by a decade and fill the gap between ground-based and space-based instruments.

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I. INTRODUCTION

Gravitational wave (GW) detection remains one of the challenges in fundamental physics and astrophysics. State-of-the-art GW detectors consisting of giant Fabry-Perot Michelson interferometers [1–5] now reach a sensitivity that justifies the expectations for a direct detection of GWs in the next few years [6]. Nevertheless, low frequency GW sources will remain hidden for ground based detectors for which the observation bandwidth will be limited to frequencies above a few Hz [7]. Reaching sub-Hz sensitivities would provide a decisive asset to GW astronomy as the sources in this band produce more powerful and durable signals [8]. For this purpose, hybrid detectors based on two distant atom interferometers (AIs) interrogated by a laser propagating over a long baseline have been proposed (see, e.g., Ref. [9]). Using as test masses free falling atoms instead of suspended mirrors could resolve most of the technical limitations presented by optical GW detectors at low frequency, such as residual seismic noise or thermal noise of suspension systems.

Like all ground based detectors, current atom interferometry proposals will nevertheless suffer from the so-called Newtonian noise (NN) [10]. NN consists in fluctuations of the terrestrial gravity field which creates a tidal effect on separated test masses and is indiscernible from the effect of a GW [10,11]. NN is therefore considered as a fundamental limit for any ground based GW detectors at frequencies below a few Hz. Various methods have been considered to circumvent this problem [12–15]. In this paper we propose a new concept which uses an array of AIs configured to reject the NN.

Unlike previous single strainmeter or gradiometer proposals where the NN and the GW signal are indiscernible, the array of AIs allows us to extract the GW signal by averaging over several realizations of the NN. The NN rejection can be further enhanced by exploiting the correlation spatial behavior of the gravity acceleration. With the 3–4 km baseline of current best optical detectors, our method reaches a NN rejection of about 2; this factor is comparable to what was obtained by other passive methods (e.g., Ref. [14]). The principle of such rejection can be tested in current AI array projects [16]. We focus here on a 16 km baseline detector that takes full advantage of our method and enables strong NN rejection by more than a decade. This could complement the current optical interferometers development program by opening the ~0.3–3 Hz observation window.

II. PRINCIPLE

A single AI gradiometer [Fig. 1(a)] consists of two AIs separated by a baseline $L$ and interrogated by a common laser beam of frequency $\nu$ close to the atomic transition frequency (see, e.g., Ref. [9]). We consider a three light-pulse AI (with $T$ the time between the successive pulses) using Bragg diffraction of atoms from a standing wave produced by retroreflecting the interrogation laser. The
output phase of each AI originates from the local phase difference $\Delta \phi$ between the two counterpropagating beams at the time of the pulse and the position of the atom [17]. The retroreflection configuration gives immunity to laser phase noise induced by position noise of the input laser system. We consider large momentum transfer (LMT) diffraction [18], where the atom absorbs $n$ photons from one beam and emits $n$ photons in the counterpropagating beam. When the interrogation laser is pulsed, the atom undergoes diffraction with a momentum change of $n \times 2 \hbar k$ along the laser propagation direction ($k = 2 \pi \nu / c$ is the laser wave vector). A phase $n \Delta \phi(X, t)$ is imprinted on the diffracted component.

After the three pulses, the output phase of the AI reads

$$\Delta \phi(x, t) = e(X, t) + 2nk \left[ \frac{\Delta \nu(t)}{\nu} + \frac{\hbar(t)}{2} \right] (L - X) + \Delta x_2(t) - \Delta x(X, t) \otimes s(t)$$

(1)

where $e(X, t)$ represents the detection noise (e.g., atom shot noise) on the output phase of an AI using atoms placed at position $X$. Here, $s(t)$ is the sensitivity function of the three pulse AI [19], and it relates the AI output phase to the second temporal derivative of the local laser phase difference $\Delta \phi$. $\Delta x_2(t)$ is the position noise of the retroreflecting mirror, and $\Delta x(X, t)$ represents the motion of the atoms along the laser beam direction due to the fluctuations of the local gravitational acceleration.

Taking the differential phase $\psi(X, t) = \Delta \phi_2(X, t) - \Delta \phi_2(X + L, t)$ between two AIs separated by the distance $L$ and neglecting laser frequency noise yields

$$\psi(X, t) = 2nk \left[ \frac{\dot{L}}{2} + a_x(X + L, t) - a_x(X, t) \right] \otimes s_a(t) + e(X, t) - e(X + L, t),$$

(2)

where $s_a(t)$ is the AI sensitivity function to acceleration, given by $\ddot{s}_a(t) = s(t)$. Importantly, position noise $\Delta x_2(t)$ of the retroreflecting mirror has been rejected in this gradiometer configuration. Equation (2) shows that fluctuations of the local gravity field result in an acceleration signal $a_x(X, t) = \dot{\Delta} x(X, t)$ whose gradient will have the same signature as that of the GW (see Ref. [17] for a more rigorous calculation).

The differential phase of Eq. (2) can be written as $\psi(\tilde{\eta}) = H(t) + \tilde{\eta}(t)$, where $H(t)$ is the GW signal and $\tilde{\eta}(t)$ the noise (detection noise and NN) at position $X$. Our idea is to extract $H(t)$ using a Monte Carlo method: The GW signal is obtained by averaging over several samples of the noise $\tilde{\eta}(t)$, which formally reads $H = \frac{1}{N} \sum_i \psi_i(t)$ of the single gradiometer and compute the average signal

$$H_N(t) = \frac{1}{N} \sum_{i=1}^{N} \psi_i(t),$$

(3)

which represents a nonbiased approximation to the GW signal of interest, i.e., $Lh(t)/2$. Assuming that the $N$ realizations are independent, the residual noise on the GW measurement is reduced by $\sqrt{N}$,

$$\sigma_H = \frac{\sqrt{2} \sigma_\eta}{\sqrt{N}},$$

(4)

with $\sigma_\eta = \sqrt{\sigma_a^2 + \sigma_e^2}$ the standard deviation (s.d.) resulting from the NN and detection noise which we considered as independent variables of s.d., $\sigma_a$ and $\sigma_e$, respectively. We assumed uncorrelated noise between the 2 AIs of a single gradiometer, yielding $\sqrt{2}$. This is always valid for the detection noise and applies for the NN when the gradiometer baseline $L$ is much larger than the NN correlation length. Since the GW signal increases with $L$, a very long gradiometer baseline will be considered in the following, which validates the assumption of uncorrelated NN between the two AIs. As the $N$ gradiometer measurements are assumed to be independent, the AI array brings a $\sqrt{N}$ rejection factor for the NN (and for the detection noise).

We study an implementation of this Monte Carlo sampling method in which $N$ different gradiometer measurements are simultaneously realized in parallel thanks to an array of spatially distributed AIs. The proposed configuration is chosen to enhance the NN reduction via variance reduction [20]. For that, we optimize the AI array distribution, i.e., the signal spatial sampling, in order to benefit from the spatial behavior of NN correlations. We show that, in a given
frequency band, a significant additional rejection factor can be gained with respect to the standard $\sqrt{N}$ of Eq. (4).

III. IMPLEMENTATION AND SENSITIVITY OF THE DETECTOR

The implementation is sketched in Fig. 1(b). We consider a symmetric configuration consisting of two orthogonal arms of the same length and interrogated by the same laser. For a GW with (+) polarization, laser frequency noise is therefore rejected (see Appendix A for more details). Each arm of total length $L_a$ consists in a series of gradiometers of baseline $L = X_{N+i} - X_i$ which are separated by the distance $\delta$. The geometrical parameter $\delta_N$ reflects that the baseline $L$ and the separation $\delta$ between the gradiometers are independent. For $1 \leq i \leq N$ we define

$$\psi_i(t) = [\Delta \phi_i(X_i, 0, t) - \Delta \phi_i(X_{N+i}, 0, t)]$$

$$- [\Delta \phi_i(0, Y_i, t) - \Delta \phi_i(0, Y_{N+i}, t)]$$

(5)

and compute the output signal $H_N(t)$ of the detector using Eq. (3). It contains the GW signal $h(t)$, as well as the detection noise $\epsilon(t)$ and the NN $\alpha(X, t)$. To derive the detector strain sensitivity curve, e.g., the minimum detectable GW power spectral density (PSD) $S_h(\omega)$ [21,22], we compute the PSD of the detector output, $S_{H_N}(\omega)$, using Eqs. (2), (3), and (5):

$$S_{H_N}(\omega) = (2nkL)^2 \omega^4 S_h(\omega) |\hat{\delta}_a(\omega)|^2$$

$$+ (2nk)^2 S_a(\omega) |\hat{\delta}_a(\omega)|^2 + \frac{4S_c(\omega)}{N}. \quad (6)$$

Here $\hat{\delta}_a(\omega) = 4\sin^2(\omega T/2)/\omega^2$ is the Fourier transform of the AI sensitivity function to acceleration $\delta_a(t)$, and $S_c(\omega)$ is the PSD of the detection noise. The reduction by the factor $N$ reflects the uncorrelated detection noise in the different AIs. The ratio between the first term (the GW contribution) and the last two terms (the noise PSD) of Eq. (6) defines the SNR of our detection. If we consider a minimum sensitivity with a SNR of 1, we obtain the strain sensitivity function

$$S_{a}(\omega) = \frac{S_h(\omega)}{\omega^4 L^2} + \frac{4S_c(\omega)}{16NL^2(2nk)^2 \sin^4(\omega T/2)}. \quad (7)$$

The NN PSD $S_a(\omega)$ contains two contributions: one given by the gravity acceleration correlations between AIs at two positions $\{X_i, X_j\}$ in the same arm, and one given by the correlations between AIs at two positions $\{X_i, Y_j\}$ in orthogonal arms. The calculation of these contributions is detailed below.

Before looking into the details of the AI array rejection method, we review the sources of NN, which are related to the modification of the mass distribution around the detector. We focus on the two main sources previously identified for ground based detectors: (i) seismic noise related to elastic waves propagating within the ground [10,23,24] (seismically induced Newtonian noise—SNN), and (ii) air mass fluctuations in the near atmosphere [10,25]. We base our calculation on the Saulson model [10]: For each frequency $f = \omega/2\pi$, the ground is subdivided into cells of fluctuating density whose size corresponds to the half wavelength $\lambda_p(\omega) = v_a/2f$ of a propagating compression wave of velocity $v_a$. More specifically, we use an upgrade of the Saulson model that guarantees the mass conservation by assuming an ant correlation between adjacent cells [23]. We plot in Fig. 2 the spatial behavior of the gravity acceleration correlation between two distant points. Mass conservation yields a negative minimum of the correlation function for a characteristic length, which has been reported for the seismic noise in Ref. [26]. The main other sources of low frequency NN are those related to air pressure fluctuations caused by wind induced air turbulence [10] (Infrasound Newtonian Noise, INN), and to the effect of turbulence induced frozen cells of random temperature dragged by the wind [25]. For a detector at depth $H$, the latter effect has a cutoff frequency $f_c = v_{wind}/(4\pi H)$ [25] which is out of the detector band for $H > 100$ m ($v_{wind} = 10 - 20$ m/s is the wind velocity).

We now give some details on the calculation of the NN contribution $S_{ai}(\omega)$ appearing in Eq. (7), which we express as

$$S_{a}(\omega) = \frac{2N\Sigma_{i,j=1}^{N}}{N^2} \Sigma_{i,j=1}^{2N} C_{||}(X_i, X_j, \omega) + \frac{2N\Sigma_{i,j=1}^{2N}}{N^2} \Sigma_{i,j=1}^{2N} C_{\perp}(X_i, Y_j, \omega),$$

(8)

with the single arm component

$$\Sigma_{i,j=1}^{2N} \Sigma_{i,j=1}^{N} C_{||}(X_i, X_j) \equiv 4 \Sigma_{i,j=1}^{N} C_{xx}(X_i, X_j) - 4 \Sigma_{i,j=1}^{N} C_{xx}(X_i, X_{j+N}).$$

(9)

FIG. 2. Spatial behavior of the normalized NN correlations between two distant points separated by the relative distance $x = |X_j - X_i|/\lambda_p(\omega)$, where $\lambda_p(\omega)$ is the NN correlation length. The anticorrelation is a consequence of mass conservation between adjacent cells of fluctuating density.
and the crossed arms component

\[ \sum_{i,j}^{2N} C_{ij}(X_i, X_j) \equiv -2 \sum_{i,j}^{N} C_{xy}(X_i, Y_j) - 2 \sum_{i,j}^{N} C_{xy}(X_{i+N}, Y_{j+N}) + 4 \sum_{i,j}^{N} C_{xy}(X_{i+N}, Y_j). \]

In Eqs. (9) and (10), \( C_{xy} \) is the Fourier transform of the gravity acceleration correlation function between two AIs in arms \((x, y)\), and we hid the \( \omega \) dependency for clarity. We assumed isotropy of the NN and that the detector is surrounded by a homogeneous medium for both seismic and infrasound-air density fluctuations. We also consider the effects of the SNN isotropy of the NN and that the detector is surrounded by a spatial behavior of NN correlations between two points in the same arm is given by

\[ C_{xx}^{(u,a)}(X_i, X_j, \omega) = G^2 \mathcal{L}_\rho^{(u,a)}(\omega)^2 \Delta \rho_u^{2(a)}(\omega) J(Y_{ij}(\omega)), \]

with \( x_{ij}^{(u,a)}(\omega) = \frac{|X_i - X_j|}{\mathcal{L}_\rho^{(u,a)}(\omega)} \). Here \( G \) is the gravitational constant, \((u, a)\) are indices denoting the seismic and infrasound NN contribution, and \( \mathcal{L}_\rho^{(u,a)}(\omega) = \pi v_u v_a / \omega \) is the corresponding correlation length, with \( v_u \) and \( v_a \) being, respectively, the speed of seismic waves in the underground and the speed of sound in the air. The function \( J(x) \) is a 3D integral which represents the spatial behavior of NN correlations between two distinct points \( X_i, X_j \). It is represented in Fig. 2 against the relative distance \( x \). A similar expression as in Eq. (11) holds for \( C_{xy} \), the correlation between two points \( \{X_i, Y_j\} \) in orthogonal arms.

Following Refs. [8,10], the density fluctuations for SNN and INN are respectively given by \( \Delta \rho_u^{2(a)}(\omega) = \frac{\rho_u^2}{\pi r^2} \Delta \rho_u(a) \) and \( \Delta \rho_u^{2(a)}(\omega) = \frac{\rho_u}{r^2} \Delta \rho_u(a) \). Here \( \rho_u = 2300 \text{ kg/m}^3 \) is the mean underground density, \( \Delta \rho_u(a) \) the seismic acceleration noise, \( \rho_u = 1.3 \text{ kg/m}^3 \) the mean air density, \( 1/\gamma^2 = 1/2 \) the air coefficient of adiabatic compression, \( p_u \) the air pressure and \( \Delta p^2(a) \) its PSD. We consider seismic waves with a typical speed for \( P \) waves of \( v_u = 2 \text{ km/s} \) corresponding, for example, to porous rocks [27], yielding \( L_u = 1 \text{ km at 1 Hz} \). The air pressure fluctuation spectrum used for the INN is \( \Delta p^2(a) = 0.3 \times 10^{-5} \text{ (f/1 Hz)}^2 \text{Pa}^2 / \text{Hz} \) (as used by Saulson [10]). The seismic noise for the SNN is \( 1 \times 10^{-17} \text{ m}^2 \text{ s}^{-4} / \text{Hz} \) at 1 Hz as often reported in underground sites (see, e.g., Ref. [28,29]).

The gradiometer separation \( \delta \) determines the NN rejection efficiency. For instance, if \( \delta \) is much larger than the NN correlation length \( L_u(\omega) \) for all \( \omega \), then the successive measurement points are uncorrelated and Eq. (8) reduces to terms \( i = j \), yielding

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SNN, yielding a shot noise limited strain sensitivity level of \(3 \times 10^{-23}/\sqrt{\text{Hz}}\) at 2 Hz. At low frequency (\(\lesssim 0.3\) Hz), the SNN correlation length becomes much greater than \(\delta\), which results in a high correlation between the different gradiometer measurements, thereby preventing the NN rejection. At high frequencies (>2 Hz), the detector is limited by detection noise.

**IV. DISCUSSION**

As shown in Fig. 4, such performances would allow observations in the frequency band \(\sim 0.3 - 3\) Hz. This frequency band is covered neither by existing detectors nor by next generation detectors such as the Einstein Telescope [7] or ESA’s L3 gravity observation mission eLISA [32], despite the presence of several astrophysical sources [33].

To conclude, we show that an array of AIs in an appropriate configuration can allow ground based GW detection in the \(\sim 0.3 - 3\) Hz decade by overcoming the current limitation imposed by NN. The main idea consists in using a distribution of long baseline AI gradiometers to average the NN to zero. We show that a further NN reduction can be achieved by exploiting the NN correlation properties to configure the AI array. While the present concept can be tested on existing apparatuses, our method will take full advantage of the recent and future developments in atom interferometry. More advanced schemes might also lead to sensitivity improvements. For example, the measurement of higher order spatial derivatives of the gravity field [34], or the implementation of more complex spatial distributions of AIs, could achieve higher

![Fig. 4](image1.png)

**FIG. 4.** The strain sensitivity of the proposed AI array covers the frequency region \(\sim 0.3 - 3\) Hz, where future ground-based (Einstein Telescope, ET) and space-based (eLISA) detectors are blind. The dashed line represents an envelope of the proposed AI array sensitivity function at frequencies above 3 Hz and corresponds to an average detector response for different interrogation times \(T\).

![Fig. 5](image2.png)

**FIG. 5.** Noise rejection factor of the SNN (top) and the INN (bottom) for the implementation of the AI array described in the main text.

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**APPENDIX A: REQUIREMENT ON SEISMIC ISOLATION OF BEAM SPLITTING OPTICS**

In the proposed configuration consisting of two orthogonal arms [Fig. 1(b)], the beam splitting optical system that distributes the laser to the two arms introduces an asymmetry. Position noise (e.g., seismic noise) of the splitting optics results in laser frequency noise which will affect one arm and not the other: The phase \(\phi_L\) of the laser beam propagating in the \(y\) direction picks up the position noise \(\delta y\) of the splitting optics, which results in a frequency noise contribution \(\Delta \nu = \frac{1}{2\pi} \frac{d\phi_L}{dt} = kf\delta y\) (with Fourier frequency \(f\)). According to Eq. (1), such frequency noise yields a...
contribution to the relative phase signal of the AI gradiometers in the y arm equal to $2nkL \times \Delta u(t)/\nu = 2nkL \times 2\pi f \delta y/c$, to be compared with the GW signal $2nk \times Lh$. Considering a minimum sensitivity with a SNR of 1 yields the requirement on the position noise $\delta y_{\text{min}}$ of the splitting optics given by $\delta y_{\text{min}} = \hbar c/2\pi f$. To reach a detector peak sensitivity of $3 \times 10^{-23}/\sqrt{\text{Hz}}$ at $f = 2 \text{ Hz}$, the seismic noise must be below $\delta y_{\text{min}}(2 \text{ Hz}) \approx 7 \times 10^{-16} \text{ m}/\sqrt{\text{Hz}}$. At $f = 0.3 \text{ Hz}$, the AI array can feature a sensitivity of $1 \times 10^{-19}/\sqrt{\text{Hz}}$ if the seismic noise is mitigated below $\delta y_{\text{min}}(0.3 \text{ Hz}) \approx 2 \times 10^{-11} \text{ m}/\sqrt{\text{Hz}}$. Such seismic noise levels can be obtained with a dedicated low frequency suspension system (see, e.g., Ref. [35]). Finally, the contribution resulting from NN induced position fluctuations of the splitting optics is negligible at the targeted sensitivity level.

**APPENDIX B: NEWTONIAN NOISE REJECTION EFFICIENCY**

Figure 5 illustrates the NN rejection efficiency of the AI array. The dashed line shows the rejection in the case of a standard Monte Carlo average illustrating the $\sqrt{80}$ rejection factor. The plain line shows the rejection using the Monte Carlo variance reduction method exploiting the spatial behavior of the gravity acceleration correlation function. The maximum rejection is obtained when the NN correlation length $L_{\phi}^{(\rho,0)} = \nu_{\phi,0}/2f$ approaches the distance corresponding to the anticorrelation of the gravity acceleration correlation function, which, from Fig. 2, is obtained for $\lambda_{\phi,0} \approx 1.3$. This condition on the length translates in the frequency where the maximum rejection is observed, given by $f = \nu_{\phi,0}\lambda_{\phi,0}/2\delta$, and equals 1.1 Hz for the INN and 6.5 Hz for the SNN.

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