Research Article

Design of a Data-Driven Controller with Evaluating Controller Performance

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1. INTRODUCTION

In most industries, it is very important to get desired control performance. Data-driven control schemes [1–4] have been proposed to achieve the aforementioned desired control performance without using any system identifications. For time-variant systems, performance-driven controller [5] has been proposed to improve the steady state control performance only when the performance is poor. However, performance-driven controller cannot evaluate the transient state because this scheme focuses on the variance of steady state error.

In this paper, the scheme of evaluating controller performance without using any system identifications is proposed. According to the proposed scheme, the control performance calculator and controller design are integrated using only input and output data.

2. OUTLINE FIGURE OF THE PROPOSED SCHEME

The schematic figure of the proposed control system is shown in Figure 1. $C(z^{-1})$, $G(z^{-1})$, $G_n(z^{-1})$, and $\hat{G}(z^{-1})$ are the controller, controlled system, reference model and estimated system model, respectively.

The purpose of the proposed control system is to achieve the desired control performance by minimizing the following criterion $J$, [Equations (1) and (2)]:

\[
J = \frac{1}{2} \phi(t)^2
\]

\[
\phi(t) = y(t) - y_r(t),
\]

where $y(t)$ and $y_r(t)$ are the control output and reference output, respectively.

Another purpose of the proposed scheme is to design the estimated system model $G(z^{-1})$ by minimizing the following Equations (3) and (4):

\[
\hat{J} = \frac{1}{2} \tilde{\phi}(t)^2
\]

\[
\tilde{\phi}(t) = \hat{y}(t) - \hat{y}(t),
\]

where $\hat{y}(t)$ is the estimated output. In the proposed scheme, $\hat{G}(z^{-1})$ can be introduced by using the controller parameters and reference model parameters without any system identifications. Therefore, controller and estimated system model can be designed simultaneously.

In addition, users set a desired reference model expressed by the following Equations (5) and (6):

\[
y_r(t) = G_n(z^{-1})r(t)
\]

\[
G_n(z^{-1}) = \frac{z^{-(1-d)}P(1)}{P(z^{-1})}
\]

where $r(t)$ is the reference signal and $P(z^{-1})$ is user-specified polynomial. $P(z^{-1})$ is designed based on the reference design [6] as follows [Equations (7) and (8)]:

\[
P(z^{-1}) = 1 + p_1 z^{-1} + p_2 z^{-2}
\]
3. RELATIONSHIP BETWEEN CONTROLLER AND ESTIMATED SYSTEM MODEL

The following Equation (9) can be obtained by introducing the optimized controller \( C(z^{-1}) \) which achieves \( \phi_E(t) = 0 \):
\[
\frac{G(z^{-1})C(z^{-1})}{1 + G(z^{-1})C(z^{-1})} = G_n(z^{-1}).
\]
(9)

The controlled system \( G(z^{-1}) \) is expressed as follows by using the aforementioned Equation (10):
\[
G(z^{-1}) = \frac{G_n(z^{-1})}{C(z^{-1})[1 - G_n(z^{-1})]}.
\]
(10)

Here, the following estimated system model \( \tilde{G}(z^{-1}) \) is defined using a controller \( C(z^{-1}) \) instead of \( C(z^{-1}) \) because it is difficult to obtain the optimized controller \( C(z^{-1}) \) [Equation (11)]:
\[
\tilde{G}(z^{-1}) = \left[ \frac{G_n(z^{-1})}{C(z^{-1})[1 - G_n(z^{-1})]} \right].
\]
(11)

Note that the estimated controlled system \( \tilde{G}(z^{-1}) \) is expressed using a controller \( C(z^{-1}) \) and reference model \( G_n(z^{-1}) \) without any system identifications.

\( \tilde{G}(z^{-1}) \) equals to \( G(z^{-1}) \) when the optimized controller \( C(z^{-1}) \) is obtained. It mentions that \( \phi_E(t) = 0 \) because of \( G(z^{-1}) = G(z^{-1}) \). Therefore, the optimized controller \( C(z^{-1}) \) achieves \( \phi_E(t) = 0 \) and \( \phi(t) = 0 \) simultaneously.

### 3.1. Evaluation of the Controller Performance

The optimized controller \( C(z^{-1}) \) makes \( \phi(t) = 0 \). In contrast, \( \phi(t) \) becomes large when the performance of the controller \( C(z^{-1}) \) is poor. Hence, this paper considers the performance of the controller \( C(z^{-1}) \) based on \( \phi(t) \).

### 3.2. Tuning Scheme of the PID Gains

In this paper, the controller is utilized as following I-PD controller [Equations (12) and (13)]:
\[
\Delta u(t) = K_p e(t) - K_i \Delta y(t) - K_d \Delta^2 y(t)
\]
(12)
\[
e(t) = r(t) - y(t),
\]
(13)

where \( K_p, K_i \) and \( K_d \) are the proportional gain, integral gain and derivative gain, respectively.

The estimated system model \( \tilde{G}(z^{-1}) \) is expressed by using I-PD controller as follows [Equation (14)]:
\[
\tilde{G}(z^{-1}) = \frac{G_n(z^{-1})}{K_p - C(z^{-1})G_n(z^{-1})},
\]
(14)

where \( C(z^{-1}) \) is as follows [Equation (15)]:
\[
C(z^{-1}) = \frac{K_p + K_i + K_d \Delta^2}{\Delta}.
\]
(15)

The estimated output is calculated as follows [Equation (16)]:
\[
\hat{y}(t) = \frac{G_n(z^{-1})}{K_p - C(z^{-1})G_n(z^{-1})} u(t),
\]
(16)

where \( u(t) \) is control input. To apply the least squares method, \( \phi(t) = 0 \) is considered and the following Equation (17) is derived by using Equations (2) and (18):
\[
\Delta G_n(z^{-1}) u(t) = K_p \Delta y(t) - \frac{K_i}{\Delta} \Delta (t) - \frac{K_d}{\Delta} \Delta y(t).
\]
(17)

Therefore, the PID gains are calculated by using the following least squares method [Equations (19) and (20)]:
\[
\theta = (\Phi^T \Phi)^{-1} \Phi^T \psi,
\]
(19)
\[
\psi(t) = \begin{bmatrix} -\Delta G_n(z^{-1}) y(t) \\ (1 - G_n(z^{-1})) y(t) \\ -\Delta G_n(z^{-1}) y(t) \end{bmatrix},
\]
\[
\Phi = \begin{bmatrix} \psi(1) & \psi(2) & \cdots & \psi(N) \end{bmatrix},
\]
\[
v = \begin{bmatrix} \Delta G_n(z^{-1}) u(1), \cdots, \Delta G_n(z^{-1}) u(N) \end{bmatrix}^T,
\]
\[
\theta = \begin{bmatrix} K_p, K_i, K_d \end{bmatrix}.
\]
(20)
4. NUMERICAL EXAMPLE

The controlled system \( G(s) \) is given as follows [Equation (21)]:

\[
G(s) = \begin{cases} 
\frac{1}{1+10s} & (t < 100) \\
\frac{2}{1+20s} & (t \geq 100) 
\end{cases}
\]  

(21)

The parameters of the reference model \( G_m(z) \) are set as follows [Equation (22)]:

\[
\sigma = 3.0, \delta = 0.
\]  

(22)

Finally, the initial PID gains are set as follows [Equation (23)]:

\[
K_p = 1.0, K_i = 1.0, K_d = 1.0.
\]  

(23)

In this section, the following three simulations are shown.

A) Figure 2: Control result by using initial PID gains of Equation (23).

B) Figure 3: Control result of the proposed scheme without controller retuning.

C) Figure 5: Control result of the proposed scheme with controller retuning.

4.1. Control Results

Figure 2 shows the control result by using initial PID gains of Equation (23). The control performance is poor because control output \( y(t) \) does not track to reference output \( y_r(t) \).

Figure 3 shows the control result of the proposed scheme. The following PID gains [Equation (24)] were calculated applying Equation (19) by using the data between \( t = 0 \) and 100 [step] in Figure 2:

\[
K_p = 6.74, K_i = 2.49, K_d = 0.0.
\]  

(24)

In Figure 3, the control performance is good even though the system \( G(z) \) is changed at \( t = 100 \) [step]. It mentions that it is difficult to detect the system parameters are changed. The reason for the abovementioned, the feedback controller \( C(z) \) has an integrator, and it can reduce the steady state error. On the other hand, Figure 4 shows the trajectories of the estimated output \( \hat{y}(t) \). It easier to detect the system parameters are changed than Figure 3.

Finally, Figure 5 shows the control result with controller retuning at 120 [step]. Figure 6 shows the estimated output \( \hat{y}(t) \), and Figure 7 shows the trajectories of the PID gains corresponding to Figure 5. In Figure 7, each PID gains are slightly adjusted, however, the estimated output \( \hat{y}(t) \) of Figure 6 is significantly improved. Therefore, the proposed scheme can diagnose the system parameters are changed strictly.
5. CONCLUSION

This paper has proposed the design of data-driven control system with evaluating controller performance. The features of the proposed scheme are as follows:

- Controller and estimated system model can be designed simultaneously.
- Controller performance is evaluated by the error between output $y(t)$ and estimated output $\hat{y}(t)$ without using any system identifications.

The proposed scheme has been verified by numerical examples.

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