Gravitational radiation in Infinite Derivative Gravity
and connections to Effective Quantum Gravity

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The Hulse-Taylor binary provides possibly the best test of GR to date. We find the modified quadrupole formula for Infinite Derivative Gravity (IDG). We investigate the backreaction formula for propagation of gravitational waves, found previously for Effective Quantum Gravity (EQG) for a flat background and extend this calculation to a de Sitter background for both EQG and IDG. We put tighter constraints on EQG using new LIGO data. We also find the power emitted by a binary system within the IDG framework for both circular and elliptical orbits and use the example of the Hulse-Taylor binary to show that IDG is consistent with GR.

General Relativity (GR) has been spectacularly successful in experimental tests, notably in the recent detection of gravitational waves [1]. One of the most renowned tests is the Hulse-Taylor binary. The way the orbital period of these two stars changes over time depends on the gravitational radiation emitted. This matches the GR prediction to within 0.2% [2].

However, GR breaks down at short distances where quantum effects start to play a role. The propagator $\Pi_{\mathrm{IDG}}$ around a flat background in terms of the spin projection operators is modified as follows [6]

$$\Pi_{\mathrm{IDG}} = \frac{P^2}{a(k^2)} + \frac{P^0}{a(k^2) - 3c(k^2)} = \frac{\Pi_{\mathrm{GR}}}{a(k^2)},$$

where $a$ and $c$ (given in [7]) are combinations of the $F_i(\Box)$s from [4]. In the second equality we have taken the simplest choice $a(k^2) = c(k^2)$, giving a clear path back to GR in the limit $a(k^2) \to 1$.

The simplest way to show that there are no ghosts is to show that there are no poles in the propagator, which means there can be no zeroes in $a(k^2)$. Any function with no zeroes can be written in the form of the exponential of an entire function, so we choose $a(k^2) = c(k^2) = \exp[\gamma(k^2/M^2)]$, where $\gamma$ is an entire function.

Any entire function can be written as a polynomial $\gamma(k^2) = c_0 + c_1 k^2 + c_2 k^4 + \cdots$, so a priori we have an infinite number of coefficients to choose. However, it was shown that only the first few orders will appreciably affect the predictions of the theory, as terms higher than order $\sim 10$ can be described by a rectangle function with a single unknown parameter $\delta^3$.

The quadrupole formula tells us the perturbation to a flat metric caused by a source with quadrupole moment $I_{ij}$. Here we use the equations of motion to find the modified quadrupole formula for IDG.

## I. Modified Quadrupole Formula

The IDG equations of motion for a perturbation $h_{\mu\nu}$ around a flat background $\eta_{\mu\nu}$ are given by [6]

$$-\kappa T_{\mu\nu} = \frac{1}{2} \left[ a(\Box) \left( \Box h_{\mu\nu} - \partial_\rho \left( \partial_\rho h^\rho_\mu + \partial_\rho h^\rho_\nu \right) \right) + c(\Box) \left( \partial_\rho \partial_\sigma h + \eta_{\mu\rho} \partial_\sigma \partial_\tau h^\sigma_\tau - \eta_{\mu\nu} \Box h \right) + f(\Box) \partial_\rho \partial_\sigma \partial_\tau \partial_\gamma h^\gamma_\tau \right],$$

where $\kappa = M_p^{-2}$ and

$$a(\Box) = 1 + M_p^{-2} \left( F_2(\Box) + 2F_3(\Box) \right) \Box,$$

$$c(\Box) = 1 - M_p^{-2} \left( 4F_1(\Box) - F_2(\Box) + \frac{2}{3} F_3(\Box) \right) \Box,$$

$$f(\Box) = M_p^{-2} \left( 4F_1(\Box) + 2F_2(\Box) + \frac{4}{3} F_3(\Box) \right),$$

and it should be noted that as $a(\Box) = c(\Box)$, then $f(\Box) \Box = a(\Box) - c(\Box) = 0$. If we take the de Donder gauge $\partial_\rho h^\rho_\mu = \frac{1}{2} \partial^\nu h$ and assume $a(\Box) = c(\Box)$, then

$$-2\kappa T_{\mu\nu} = a(\Box) \Box h_{\mu\nu},$$

where $a = M_p^{-2}$ and $c = 1$.
where we have defined $\tilde{h}_{\mu\nu} \equiv h_{\mu\nu} - \frac{1}{2} g_{\mu\nu} h$. Note that in the limit $a \rightarrow 1$, we return to the GR result. We invert $a(\Box)$ and follow the usual GR method \[35\] where we assume the source is far away, composed of non-relativistic matter and isolated. In this approximation, the Fourier transform of $h_{\mu\nu}$ with respect to time is

$$\tilde{h}_{\mu\nu} = 4G e^{ikr} \int d^3y \frac{\tilde{T}_{\mu\nu}(k, y)}{a(k^2)}. \quad (6)$$

When we insert the definition of the quadrupole moment, $I_{ij} = \int d^3y T^{00}(y) g^{ij}$, write out the full expression for $\tilde{I}_{ij}$ and define the retarded time $t_r = t - r$, we obtain

$$\tilde{h}_{ij} = -G \frac{1}{r} \frac{d^2}{dt^2} \int dk dt \frac{e^{-ikr}}{a(k^2)} I_{ij}(t'). \quad (7)$$

This is the modified quadrupole formula for the simplest case of IDG. We now need to specify $I_{ij}$. For example, when we look at the radiation emitted by a binary system of stars of mass $M_s$ in a circular orbit, the 11 component of $I_{ij}$ is $I_{11}(t) = M_s R^2 (1 + \cos(2\omega t))$, where $R$ is the distance between the stars and $\omega$ is their angular velocity. Therefore

$$\tilde{h}_{11} = \frac{4GM^2 R^2}{r} \left(1 + e^{-\frac{4\omega^2}{M^2} \cos(2\omega t)}\right). \quad (9)$$

Comparing to the GR case, we see that this matches the GR prediction at large $M$, but at small $M$ there is a reduction in the magnitude of the oscillating term compared to GR.

### III. BACKREACTION EQUATION

There is a second order effect where gravity couples to itself and produces a backreaction. In \[36\], the backreaction was found for Effective Quantum Gravity (EQG). EQG has a similar action to IDG (the $F_i(\Box)$ in \[1\]) are replaced by $a_i + b_i \log(\Box/\mu^2)$ where $\mu$ is a mass scale \[37, 39\].

In this section we generalise the result of \[36\] (see also \[40, 42\]) and extend it to a de Sitter background. Using the Gauss-Bonnet identity and a similar expression for the higher-order terms \[43\] we can focus on \[1\] without the Weyl term.

Far away from the source, we use the gauge $\nabla^\mu h^\nu = 0$ and $h^0 = 0$, to simplify the linearised and quadratic (in $h_{\mu\nu}$) curvatures around a de Sitter background, given in \[A1\] and \[A2\].

The linear vacuum equations of motion around a dS background in this gauge \[44, 45\] are

$$\Box - 2H^2) F_2(\Box) h^\alpha_\nu = - (1 + 24M_p^{-2}H^2 f_{10}) \left(\Box - 2H^2\right) h^\alpha_\nu, \quad (10)$$

where $f_{10}$ is the zeroth order coefficient of $F_1(\Box)$ and the background Ricci curvature scalar is $R = 12H^2$, where $H$ is the Hubble constant. Upon inserting \[10\] into the averaged second order equations of motion for the non-GR terms \[A3\],

$$\kappa_{\nu}^{IDG} = (1 + 24M_p^{-2}H^2 f_{10}) \left[-\frac{1}{2} \langle h^\sigma_\sigma (\Box - 2H^2) h^\sigma_\nu \rangle + \frac{1}{8} \delta^\nu_\nu \langle h^\sigma_\sigma (\Box - 2H^2) h^\sigma_\nu \rangle\right],$$

where $f_{10}$ corresponds to $b_1$ in the EQG formalism and $\langle X \rangle$ represents the spacetime average of $X$ using the same definition as \[36\].

1. Alternatively, we can follow the method of \[34\] and define the gauge $\partial^\nu \gamma_{\mu\nu} = 0$, where

$$\gamma_{\mu\nu} = a(\Box) h_{\mu\nu} - \frac{1}{2} g_{\mu\nu} \epsilon(\Box) h - \frac{1}{2} \eta_{\mu\nu} f(\Box) \partial_\alpha \partial_\beta h^{\alpha\beta}. \quad (11)$$

This produces the result $-2\kappa_{\mu\nu} \nabla_{\mu\nu} = \Box \gamma_{\mu\nu}$.

2. There are extra terms due to the de Sitter background $H^2$ \[38, 39\], but to linear order in, these produce only terms which are linear in $\cos$ or $\sin$. The spacetime average therefore vanishes and there is no extra contribution to \[10\] from these terms.
are therefore interested in the two-sphere. In polar coordinates, \( n^\alpha \) becomes
\[
\frac{1}{(1 + 24M^2H^2f_{10})} \left\{ \omega^2 \epsilon^2 + 2(4\epsilon_0^2\epsilon_0 + \epsilon^2)(8H^2 + \omega^2 - k^2) \right\}, 
\]
where \( \epsilon^2 = \epsilon_\mu \epsilon^\mu \). Given the current value of the Hubble constant \( H_0 = \frac{H_0^2M^2}{10^{-119}} \). Therefore \( f_{10} \) would have to be of the order of \( 10^{115} \) for the de Sitter background in the present day to have a noticeable impact. Thus we can generally use the Minkowski background as a good approximation. In the EQG notation, \( f_{10} \) is replaced by \( b_1 \) which already has the constraint \( b_1 < 10^{61} \) so we can ignore this extra term.

For a classical wave, \( \omega^2 = k^2 \) so the term on the second line of (13) disappears for a Minkowski background. This is the case for IDG when we assume there are no extra poles in the propagator. On the other hand, EQG does have poles, so for EQG or IDG with a single pole there can be damping \( [50–53] \) and therefore \( \omega^2 \neq k^2 \).

Kuntz used LIGO constraints on the density parameter \( \Omega_0 \) as well as the constraint on the mass of the pole \( m > 5 \times 10^{13} \) GeV to constrain \( \epsilon \), the amplitude of the massive mode as \( \epsilon < 1.4 \times 10^{-33} [39] \). Since then, LIGO has found more stringent constraints of \( \Omega_0 < 5.58 \times 10^{-8} [51] \). Following the same method as [39], we divide by the critical density \( \rho_c = \frac{3H_0^2}{8\pi G} \) to find
\[
\Omega_0 = \frac{1}{2} \left( \epsilon_0^2 + \epsilon^2 \right) \frac{m^2}{H_0^2} < 5.58 \times 10^{-8} \tag{14}
\]
which we use to find a stronger constraint of \( \epsilon < 8.0 \times 10^{-34} \). This cuts the allowed parameter space nearly in half and makes it less likely that the detector [55] referred to in [39] would be able to detect this mode.

### IV. POWER EMITTED

We can use the backreaction equation to find the power radiated to infinity by a system, which is given by [35]
\[
P = \int_{S^2_\infty} t_{0\mu} n^\mu r^2 d\Omega, \tag{15}
\]
where the integral is taken over a two-sphere at spatial infinity \( S^2_\infty \) and \( n^\mu \) is the spacelike normal vector to the two-sphere. In polar coordinates, \( n^\mu = (0, 1, 0, 0) \). We are therefore interested in the \( t_{00} \) component.

In the limit \( H \to 0 \) and including the usual GR term, (11) becomes
\[
t_{\mu\nu} = \frac{1}{64\pi G} \left[ 2(\partial_\mu h^{TT}_\alpha \partial_\nu h^{\alpha 3}_T) + 4(h^{TT}_\sigma \Box h^{TT}_\nu) - \eta_{\mu\nu} (h^{TT}_\sigma \Box h^{TT}_\sigma) \right]. \tag{16}
\]
Note that \( h^{TT}_\nu = \eta_{0\nu} = 0 \), which means we can discard the second and third terms in the square bracket. The relevant term for the power becomes
\[
t_{0\mu} n^\mu = -\frac{GM^2}{32\pi^2 r^2} \left\{ \frac{d^3}{dt^3} \left( \hat{I}_{ij}(t_r) \right) \frac{d^3}{dt^3} \left( \hat{I}^{ij}(t_r) \right) \right\}. \tag{17}
\]
Note that this is the same as the GR expression, but where we have defined \( \hat{I}_{ij} = \int dt'_e e^{-M^2(t_e-t'_e)^2} I_{ij}(t'_e) \) instead of \( I_{ij} \). If we convert to the reduced quadrupole moment \( \hat{J}_{ij} \), using \( J_{ij} = I_{ij} - \delta_{ij}\delta_{kl} I_{kl} [35] \), we can use the identities \( [C1] \) from [35] to see that the power emitted by a system is
\[
P = -\frac{5}{32} I_{GR}^2 M^4 \omega^6 e^{-2\omega^2/M^2}. \tag{18}
\]
where \( \hat{J}_{ij} = \int dt'_e e^{-M^2(t_e-t'_e)^2} J_{ij}(t'_e) \). This result can then be applied to any system for which we know the reduced quadrupole moment. We will now apply it to binary systems in both circular and elliptical orbits.

#### A. Circular orbits

For a binary system of two stars in a circular orbit, the reduced quadrupole moment \( J_{ij} \) in polar coordinates is given in [35] and depends on the mass of each of the stars \( M_s \), the distance between them \( R \), and the angular velocity \( \omega^2 \) \( \frac{\pi G}{3} \). Using (18), our power is (again in the limit \( r \to \infty \)) and using \( \langle \sin^2(x) \rangle \equiv \frac{1}{2} \),
\[
P = \frac{128}{5} I_{GR}^2 \left( \frac{M^4_s \omega^6 e^{-2\omega^2/M^2}}{32} \right) \tag{19}
\]
This is the GR result with an extra factor of \( e^{-2\omega^2/M^2} \) where \( M \) is the IDG mass scale. This gives a reduction in the amount of radiation emitted from a binary system of stars in a circular orbit. Note that this factor tends to 1 in the GR limit \( M \to \infty \).

#### B. Generalisation to elliptical orbits

The power radiated by a binary system with a circular orbit is of limited applicability because in GR the power emitted is highly dependent on the eccentricity \( e \) of the orbit [60], i.e. \( P_{GR} = P_{GR}^\text{circ} F_{GR}(e) \), where \( F_{GR}(e) \) is an enhancement factor that reaches \( 10^3 \) at \( e = 0.9 \). The circular orbit is therefore unlikely to be an accurate approximation.

\[3\] The corrections to the orbital motion due to the change in the Newtonian potential from IDG will be negligible as this has already been constrained down to the micrometre scale, much shorter than the distance between the stars.
We find that

\[ P_{\text{IDG}} = P_{\text{GR}} f_{\text{GR}}(e) + P_{\text{IDG}} f_{\text{IDG}}(e), \]

where \( f_{\text{IDG}}(e) \) is a polynomial of 22nd order and so is given in the appendix. In the limit \( M \to \infty, P_{\text{IDG}} \to 0 \) and (23) returns to \( P_{\text{GR}} \). \( f_{\text{IDG}}(e) \) is plotted in Fig. 1 with a comparison to the enhancement factor for GR, \( f_{\text{GR}}(e) \).

The Hulse-Taylor binary has a period of 7.5 hours and ellipticity of 0.617. The radiation emitted from the Hulse-Taylor binary is 0.998 ± 0.002 of the GR prediction [2], which leads to the constraint \( M > 6.9 \times 10^{-49} M_\odot = 1.0 \times 10^{-21} \text{eV} \) on our mass scale \( M \), which is much weaker than previous constraints.

The previous lower bound [7] is \( \sim 0.01 \text{ eV} \) from lab-based experiments [3]. In order to produce a comparable constraint, we would need to study radiation produced from systems with orbital period [9] of less than \( 10^{-4} \) seconds. Not only do these systems have an orbital frequency much higher than LIGO and LISA will be able to probe (15-150 Hz [5] and \( 10^{-4}-10^{-1} \text{Hz} \) [9] respectively), but they would also be out of the weak-field regime we used for our calculations. Therefore lab-based experiments and CMB data are likely to provide the tightest constraints in the near future.

V. CONCLUSION

We found the modified quadrupole formula for IDG, which describes how the metric changes for a given stress-energy tensor. We generalised the backreaction formula already found for Effective Quantum Gravity (EQG) to a de Sitter background (for both EQG and IDG). We used updated LIGO results to give a tighter constraint of \( \epsilon < 8.0 \times 10^{-34} \) on the amplitude of the massive mode in EQG.

Finally, we found the power emitted by a binary system, for both circular and elliptical orbits and investigated the example of the Hulse-Taylor binary. We showed that IDG is consistent with the GR predictions.

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4 If we assume IDG is responsible for inflation we can obtain an even stronger lower bound of roughly \( 10^{14} \) GeV using Cosmic Microwave Background data [20, 29, 57].

5 The frequency of the radiation produced is twice the orbital frequency of the system [55].
Appendix A: Linearised and quadratic curvatures

The linearised Ricci curvatures around a de Sitter background are

\[ r_\mu^\nu = H^2 h_\mu^\nu - \frac{1}{2} \Box h_\mu^\nu, \quad r = 0. \tag{A1} \]

The curvatures to quadratic order are

\[ r^{(2)}_\mu^\nu = \frac{1}{4} \left( h^{\alpha\beta}\nabla_\mu \nabla_\nu h_{\alpha\beta} - 2 h_{\alpha(\nu} (\Box - 4H^2) h_{\mu)}^\alpha \right) \]

\[ r^{(2)} = -\frac{1}{4} h_\mu^\nu (\Box - 8H^2) h^{\mu\nu}. \tag{A2} \]

The averaged second order equations of motion are

\[ \kappa t_\mu^\nu_{IDG} = \frac{1}{2} \langle h_\mu^\sigma F^2 (\Box) (\Box - 2H^2)^2 h^{\sigma}_\nu \rangle - \frac{1}{8} \delta_\mu^\nu \langle h_\tau^\sigma F^2 (\Box) (\Box - 2H^2)^2 h^{\tau\sigma} \rangle. \tag{A3} \]

Appendix B: Adding a cosmological constant

It should be noted that it is possible to incorporate a cosmological constant \( \Lambda \) to the linearised equations of motion by taking the “\( \Lambda \)-gauge” \( \partial_\nu h_\mu^\nu = \frac{1}{2} \partial_\mu h - \Lambda x_\mu \) \[60\]. This adds an extra term \( \Lambda h_\mu^\nu \) onto the right hand side of \[5\]. This gives us possibilities for future work.

Appendix C: Other identities

We require the identities for integrating over a sphere \[35\]

\[ \int d\Omega = 4\pi, \quad \int n_i n_j d\Omega = \frac{4\pi}{3} \delta_{ij}, \]

\[ \int n_i n_j n_k n_l d\Omega = \frac{4\pi}{15} \left( \delta_{ij} \delta_{kl} + \delta_{ik} \delta_{jl} + \delta_{il} \delta_{jk} \right), \tag{C1} \]

to find

\[ \mathbf{J}_{xx} \approx J_{xx} - \frac{\sqrt{\pi} \mu}{24M^2 (1 + e \cos(\psi))^2} \left\{ \psi^2 \left( 4 \left( e^2 - 3 \right) \cos(2\psi) - 8e^2 - 19e \cos(\psi) + 3e \cos(3\psi) \right) \right. \]

\[ -2\psi'' \sin(\psi) \left( 2 \left( e^2 + 3 \right) \cos(\psi) + e(3 \cos(2\psi) + 5) \right) \} \tag{D3} \]

Appendix D: Elliptical orbits

Using our change of coordinates, the integral \[22\] becomes

\[ \mathbf{J}_{xx} = -\frac{\mu}{M} \int_{-\infty}^{\infty} dz \ e^{-z^2} \cos(\psi(t - \frac{z}{M})) - \frac{1}{3} \left( 1 + e \cos(\psi(t - \frac{z}{M})) \right)^2. \tag{D1} \]

We can use a Taylor expansion in \( \frac{1}{M} \) to write this as the GR expression \( \mathbf{J}_{xx} \) (the zeroeth order) plus the first order expression (which disappears as the integrand is odd) and finally the second order correction. We use the identities

\[ \int_{-\infty}^{\infty} e^{-z^2} dz = -\sqrt{\pi}, \quad \int_{-\infty}^{\infty} e^{-z^2} zdz = 0, \]

\[ \int_{-\infty}^{\infty} e^{-z^2} z^2 dz = -\frac{\sqrt{\pi}}{2}, \tag{D2} \]
We perform a similar calculation for $\hat{J}_{yy}$ to find that the full enhancement factor for the IDG term $f_{\text{IDG}}(e)$ is given by

$$
\begin{align*}
f(e)_{\text{IDG}} &= 1 - \frac{(9299 + 111168\pi)e}{12282 + 155520\pi} \left( \frac{1}{18423 + 233280\pi} (15413436\pi)e^3 + \frac{153262163 + 521885160\pi}{294768 + 3732480\pi} \right) \\
&\quad + \frac{(6051611 + 36789444\pi)e^5}{72(2047 + 25920\pi)} \left( \frac{(1347719 - 15413436\pi)e^3}{147384 + 1866240\pi} + \frac{294768 + 3732480\pi}{15(1908618 + 1108133\pi)e^7} \right) \\
&\quad + \frac{(34542449 + 556982911\pi)e^8}{65504 + 829440\pi} \left( \frac{(5826870871 + 2360357712\pi)e^9}{1152(2047 + 25920\pi)} + \frac{(37373085170 + 45561968109\pi)e^{10}}{4716288 + 59719680\pi} \right) \\
&\quad + \frac{(45892881151 + 15257013132\pi)e^{11}}{6144(2047 + 25920\pi)} \left( \frac{(68559329997 + 742716547416\pi)e^{12}}{36864(2047 + 25920\pi)} + \frac{(18923346001 + 5812048566\pi)e^{13}}{2304(2047 + 25920\pi)} \right) \\
&\quad + \frac{(1406663203279 + 148696224080\pi)e^{14}}{73728(2047 + 25920\pi)} \left( \frac{(61225325649 + 186007875390\pi)e^{15}}{73728(2047 + 25920\pi)} \right) \\
&\quad + \frac{(1879563787501 + 198263618004\pi)e^{16}}{98304(2047 + 25920\pi)} \left( \frac{(508886731499 + 33068066736\pi)e^{17}}{65536(2047 + 25920\pi)} \right) \\
&\quad + \frac{(7518767717389 + 7930544672016\pi)e^{18}}{393216(2047 + 25920\pi)} \left( \frac{(979983280457 + 2976126006240\pi)e^{19}}{1179648(2047 + 25920\pi)} \right) \\
&\quad + \frac{(15037546015045 + 15861089344032\pi)e^{20}}{786432(2047 + 25920\pi)} + O(e^{21})
\end{align*}
$$

(D4)

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