**Calculation of the Electrical Conductivity of Polymer Nanocomposites Assuming the Interphase Layer Surrounding Carbon Nanotubes**

Yasser Zare and Kyong Yop Rhee *

Department of Mechanical Engineering, College of Engineering, Kyung Hee University, Yongin 446-701, Korea; y.zare@aut.ac.ir
* Correspondence: rheeky@khu.ac.kr; Tel.: +82-31-201-2565; Fax: +82-31-202-6693

Received: 30 December 2019; Accepted: 9 February 2020; Published: 11 February 2020

**Abstract:** The interphase layer surrounding nanoparticles can reflect the tunneling effect as the main mechanism of charge transferring in polymer/carbon nanotube (CNT) nanocomposites (PCNT). In this paper, the percolation threshold, effective volume fraction of CNT, and the portion of percolated filler after percolation are expressed by interphase and CNT waviness. Moreover, the developed terms are used to suggest the influences of CNT dimensions, interphase thickness, and waviness on the electrical conductivity of PCNT by conventional and developed models. Thin and long CNT, thick interphase, and low waviness obtain a high fraction of percolated CNT. However, the highest level of effective filler fraction is only calculated by the thinnest CNT and the thickest interphase. Furthermore, both models show that the thinnest and the longest CNT as well as the thickest interphase and the least CNT waviness cause the highest conductivity in PCNT, because they positively contribute to the formation and properties of the conductive network.

**Keywords:** polymer/CNT nanocomposites; percolation threshold; interphase; waviness; electrical conductivity

---

**1. Introduction**

The addition of conductive fillers such as carbon nanotubes (CNT) and graphene can increase the electrical conductivity of polymers. The resulting materials as polymer nanocomposites can be used in sensors and electromagnetic interference shielding for electronic tools and electrostatic dissipation [1–27]. The typical conductivity of polymers ranges from $10^{-12}$ to $10^{-15}$ Siemens/m (S/m), while the electrical conductivity of CNT is in order of $10^6$ to $10^7$ S/m. So, at a critical filler concentration called percolation threshold, the electrical conductivity increases several orders of magnitude and after that, the conductivity levels off close to that of nanofiller [28,29]. At percolation threshold, the filler can begin to form a continuous conductive network in nanocomposite. The percolation level can be experimentally estimated by measurement of electrical conductivity of polymer CNT nanocomposites (PCNT) at dissimilar CNT concentrations. The shape of nanofiller can affect the percolation threshold of nanoparticles and conductivity of nanocomposites. For spherical nanoparticles, a smaller size decreases the percolation threshold [30], while for layered and cylindrical fillers, a larger aspect ratio (length per diameter) lowers the percolation threshold [31].

The main difficulty for creating the conductive nanocomposites with a low CNT content is the poor distribution of CNT, due to the tendency of nanotubes to form bundles in which nanotubes stick together with each other due to the van der Waals interaction [32]. The nanotubes combined into bundles do not participate in the percolation chains, which increases the percolation threshold. However, the experimental results show that an absolutely uniform distribution of the additive in the material is not optimal, but the percolation threshold depends on the duration of the heat
treatment [33]. In fact, the establishment of a percolation conductive chain in a nanocomposite requires a considerable time during which the filler particles are distributed over the volume of the polymer matrix [33].

Some models were proposed to explain and predict the conductivity of polymer composites. The electrical conductivity was commonly characterized by its dependence on filler concentration, because the conductivity of composites is close to that of pure polymer matrix at low filler fractions. Some models also considered the percolation threshold of filler. A known power-law model based on conventional percolation theory was suggested, which has been widely applied for electrical conductivity of PCNT after percolation threshold [30,34,35]. However, this model was developed for conventional composites, and disregards the physical aspects of nanofillers such as nano-size and large surface area per weight. Monte Carlo simulations were also used to analyze the percolation threshold [36], but it’s an expensive method, which does not express clear formulations.

The interphase as a different phase in polymer nanocomposites is commonly formed due to the outstanding surface area of nanoparticles, which causes strong interfacial interaction between polymer matrix and nanoparticles [37,38]. It was reported that the interphase regions positively affect the mechanical properties of polymer nanocomposites [39,40]. Therefore, many conventional models for mechanical performances of composites have been developed to consider the role of interphase [41,42]. In addition, it was found that the interphase regions usually diminish the percolation threshold of nanoparticles in polymer nanocomposites [43–47], because the interphase layer surrounding the nanoparticles can form a continuous network before the connection of particles. The influences of interphase percolation on the mechanical behavior of PCNT were investigated in the previous reports [44,48], while its role in electrical conductivity has not been deliberated. It seems that the interphase around nanoparticles can play the tunneling effect, which controls the electrical conductivity of PCNT. The main mechanism for charge transfer in PCNT was stated as electron tunneling, where all nanotubes are electrically connected, and electrons are transferred by the tunneling effect [49]. In other words, the near nanoparticles at a determinate tunneling distance produce the conductivity by electron hopping, while the nanotubes are not bodily linked. The tunneling mechanism depends on the distance between nanotubes, while the electrical conductivity of PCNT is only considered by networking of CNT above percolation threshold.

Some authors developed micromechanics models for electrical conductivity of PCNT accounting the waviness of CNT as well as tunneling distance [50,51], but they did not consider the formation of interphase in nanocomposites. Additionally, the roles of interphase region and CNT waviness in percolation threshold and other effective properties of nanoparticles have not been clearly reported. In this study, the influences of interphase and waviness on percolation threshold, effective volume fraction of CNT and the fraction of percolated (networked) CNT after percolation are plotted and discussed. In addition, these developed terms are applied to evaluate the electrical conductivity of PCNT by conventional and developed models. Actually, this paper clarifies the effects of CNT dimensions, interphase thickness and waviness of CNT on the levels of percolation, effective volume fraction of CNT, percolated CNT and electrical conductivity of PCNT. The present explanations may justify the very low percolation level of CNT as well as the extraordinary conductivity of PCNT, which cannot be obtained by conventional theories.

2. Theoretical Analysis

The percolation threshold for random distribution of CNT in PCNT can be expressed [52] by:

$$\phi_p = \frac{\pi R^2 l + (4/3)\pi R^3}{32 \pi (R + t)^3 \left[ 1 + \frac{3}{4} \left( \frac{l}{R + t} \right) + \frac{3}{32} \left( \frac{l}{R + t} \right)^2 \right]}$$

(1)

where “R” and “l” denote the radius and length of straight CNT, correspondingly and “t” shows the interphase thickness. Also, “u” is waviness parameter.
The waviness of CNT in PCNT commonly occurs, which decreases their effectiveness for conductivity. An equivalent tube with “l_{eq}” length can be regarded by waviness. A waviness parameter is defined as the length of straight nanotubes per equivalent length as:

\[ u = \frac{l}{l_{eq}} \]  

(2)

where \( u = 1 \) shows the straight CNT (no waviness), but a higher “u” demonstrates the extent of waviness.

The CNT and surrounding interphase can be assumed as effective particles, which manage the electrical conductivity of PCNT. The effective volume fraction of straight CNT is expressed [52] by:

\[ \phi_{ef} = \frac{(R + t)^2(l + 2t)}{R^2l} \phi_f \]  

(3)

where “\( \phi_f \)” is filler volume fraction.

When the waviness of CNT is considered by the length of equivalent nanotubes, Equation (3) is modified to:

\[ \phi_{ef} = \frac{(R + t)^2(l/u + 2t)}{R^2l/u} \phi_f \approx \frac{(R + t)^2}{R^2} \phi_f \]  

(4)

Additionally, a number of nanotubes in PCNT create the conductive network after percolation point and others are still dispersed in polymer matrix. An equation was proposed to calculate the fraction of percolated CNT [52] as:

\[ f = 1 - \frac{\phi_{p}^{1/3} - \phi_{p}^{1/3}}{1 - \phi_{p}^{1/3}} \]  

(5)

When the influences of interphase and CNT waviness on percolation threshold and effective CNT concentration are considered in the above equation, it develops to the following form:

\[ f_{uw} = 1 - \frac{\phi_{uw}^{1/3} - \phi_{p}^{1/3}}{1 - \phi_{p}^{1/3}} \]  

(6)

All these parameters were mentioned in [52], but the used model is different from the current study. Generally, there are similar models in the literature, which properly fit to the experimental data of real nanocomposite samples [52–54].

Now, two conventional and developed models are suggested to investigate the effects of interphase and CNT waviness on the electrical conductivity of PCNT.

A conventional power-law model for electrical conductivity of composites above percolation threshold was suggested [55] as:

\[ \sigma = \sigma_N (\phi_f - \phi_p)^b \]  

(7)

where “\( \sigma_N \)” is CNT conduction and “\( b \)” is an exponent. The theoretical and experimental studies reported the “b” values in the 1.3–3.1 range [55]. By fitting the experimental levels of electrical conductivity to above equation, “\( \phi_p \)” and “\( b \)” values can be assessed, as reported in many studies [30,34,35].

The previous studies have indicated that the waviness decreases the conductivity of CNT [56]. Accordingly, “\( \sigma_N \)” parameter can be expressed by:

\[ \sigma_{Nu} = \frac{\sigma_N}{u} \]  

(8)
So, Equation (7) can be developed by substituting of Equations (8), (4) and (1) for CNT conductivity, effective filler fraction and percolation threshold, respectively as:

$$\sigma = \sigma_{\text{Nu}} (\phi_{\text{eff}} - \phi_p)^b$$

which enables the classical model to estimate the electrical conductivity of PCNT.

Deng and Zheng [51] also suggested a model for electrical conductivity of PCNT above percolation containing haphazardly straight CNT as:

$$\sigma = \sigma_0 + \frac{f \phi_f \sigma_{\text{Nu}}}{3}$$

where “$\sigma_0$” as the electrical conductivity of polymer matrix can be disregarded, due to its very low level. This model has expressed the proper predictions for electrical conductivity of PCNT [50,51]. When the interphase and waviness of CNT are taken into account by “$f_{\text{wu}}$”, “$\phi_{\text{piu}}$” and “$\sigma_{\text{Nu}}$” terms, this model is developed to:

$$\sigma = \frac{f_{\text{wu}} \phi_{\text{eff}} \sigma_{\text{Nu}}}{3}$$

The tunneling properties can be assumed in the developed model by a tunneling parameter (T) as:

$$\sigma = \frac{T f_{\text{wu}} \phi_{\text{eff}} \sigma_{\text{Nu}}}{3}$$

which can easily calculate the electrical conductivity of PCNT by the properties of CNT, interphase, tunneling space and network. The nanocomposites containing all types of polymers (thermoplastics to elastic) and CNT (MWCNT, SWCNT or DWCNT or modified ones) can fit to this equation. Also, this model accurately fits to the experimental data of samples containing low CNT concentrations, because a high filler concentration increases the agglomerates [57].

3. Results and Discussion

The calculations of the developed model (Equation (12)) are compared to the experimental data of some samples. Two samples including epoxy/MWCNT (R = 8 nm, l = 30 μm, u = 1.2 and $\phi_p = 0.0002$) from [55] and ultrahigh molecular weight polyethylene (UPE)/MWCNT (R = 8 nm, l = 8 μm, u = 1.2 and $\phi_p = 0.0007$) from [58] are considered. When the percolation threshold of samples is fitted to Equation (1), the interphase thickness is calculated as 7 and 8 nm for epoxy/MWCNT and UPE/MWCNT samples, respectively. When these results are considered in Equation (12), the conductivity of the samples at different CNT concentrations is calculated ($\sigma_{\text{Nu}} = 10^6$ S/m). Figure 1 displays the comparison between experimental and theoretical data using Eq. 12. It is observed that the developed model acceptably estimates the conductivity for the samples. Therefore, the developed model is capable to estimate the conductivity for the real samples. “T” is also calculated as 0.0001 and 0.00025 for epoxy/MWCNT and UPE/MWCNT samples, respectively. These results indicate that the UPE/MWCNT sample has better tunneling properties compared to the epoxy/MWCNT nanocomposite.
The influences of different parameters on the percolation threshold, effective volume fraction of CNT, the fraction of percolated filler and electrical conductivity are plotted and discussed using the mentioned equations. Contour plots show the roles of two parameters in an output at average values of other parameters. Generally, the average levels of $\phi_f = 0.02$, $R = 10 \text{ nm}$, $l = 10 \mu\text{m}$, $\sigma_N = 10^6 \text{ S/m}$, $t = 4 \text{ nm}$, $u = 1.25$ and $T = 1$ are considered for all calculations.

Figure 2 illustrates “$\phi_{eff}$” levels at different values of “$R$”, “$l$”, “$t$” and “$u$” parameters using Equation (4). According to Figure 2a, “$\phi_{eff}$” only depends on “$R$” parameter and “$l$” cannot affect it. The highest “$\phi_{eff}$” is obtained by the least “$R$”, while “$\phi_{eff}$” decreases by increment of “$R$”. The highest “$\phi_{eff}$” as 0.038 is obtained at $R = 10 \text{ nm}$, but the higher “$R$” ($R > 44 \text{ nm}$) produce the least $\phi_{eff} < 0.024$. Therefore, thin CNT cause positive effect on “$\phi_{eff}$” at the different levels of “$l$”. As known, the thin CNT introduce optimistic effects on the general properties of PCNT. Moreover, it was reported that the thin nanoparticles can produce a high level of interphase fraction in nanocomposites [59,60]. So, the thin CNT can more effectively improve the performances of nanocomposites like conductivity, due to their big surface area. However, the independence of “$\phi_{eff}$” to CNT length can be attributed to its higher levels compared to “$R$” and “$t$” parameters.

Figure 2b also demonstrates the strong effect of “$t$” parameter on “$\phi_{eff}$”, while “$u$” waviness parameter does not play a role. The highest and the lowest “$\phi_{eff}$” are calculated by the thickest and the thinnest interphase, respectively. Therefore, a thick interphase shows positive role in “$\phi_{eff}$” term. It is clear that a high level of “$t$” increases the volume of effective cylinder, which occupies a high effective volume in PCNT. Normally, a high level “$\phi_{eff}$” than “$\phi_f$” is obtained in PCNT containing interphase, due to the confident effect of interphase in the effective particles. So, a thick interphase, which is obtained by strong interfacial bonding increases the effectiveness of nanoparticles in PCNT and promotes the properties of nanocomposite. The good impacts of thick interphase on the mechanical behavior of polymer nanocomposites were also observed in the literature [38,61]. The ineffective role of “$u$” parameter in “$\phi_{eff}$” term (Figure 2b) may be due to the more significant level of equivalent length than “$R$” and “$t$” (Equation (4)). Accordingly, the “$\phi_{eff}$” parameter only depends on “$R$” and “$t$” parameters and the length and waviness of CNT do not change its level.
Figure 2. “$\phi_{eff}$” (Equation (4)) as a function of (a) “R” and “l” and (b) “t” and “u” factors.

Figure 3 exhibits the effects of different parameters on “$f_u$” term as the fraction of percolated filler above percolation threshold using Equation (6). Figure 3a indicates that the least “$f_u$” as about 0.05 is obtained at $R = 50$ nm and $l = 3$ μm, while the smallest level of “R” and $l > 10$ μm significantly improve the level of “$f_u$” to 0.28. So, the highest fraction of percolated filler is obtained by the thinnest and the largest CNT based on the networkability of thin and large CNT. In other words, the potential connection and formation of a filler network in thin and long CNT are more than thick and short ones, because they can easily find each other in PCNT. It means that the large aspect ratio of these nanoparticles causes low distance and more Head-Head and Head-Tail interaction/contact between nanotubes, which facilitate their networking. However, the random distribution of thick and short CNT in PCNT makes a high distance among nanotubes, which cannot promote the networking.

Figure 3b also observes the roles of “t” and “u” parameters on “$f_u$” ranges. The highest outputs are acquired by the high level of “t” and low “u”, where $f_u = 0.3$ is estimated at $t > 6$ nm and $u < 1.5$. However, a low “t” and great “u” result in a poor “$f_u$” demonstrating that the interphase thickness and waviness show different effects on the fraction of percolated CNT in PCNT. A high “$f_u$” is obtained by thick interphase and low waviness, whereas the thin interphase and high waviness cannot improve the “$f_u$” level. The thick interphase surrounding CNT can persuade the separated CNT with high segregation distance to connection and networking. In fact, a thick interphase approaches the nanotubes and increases the possibility of networking. As a result, the number of CNT in network phase as “$f_u$” grows by a thick interphase. Obviously, a thin interphase cannot play an effective role in PCNT, which negligibly changes “$f_u$”. On the other hand, the negative role of “u” parameter in “$f_u$” is attributed to the reduced length of CNT, which decreases the effective interaction among CNT for connection. Undoubtedly, more waved CNT (high u) produce a high level of segregation distance between nanotubes in PCNT, which decreases the probability of networking. Accordingly, the waved CNT negatively affected the joining of nanotubes and production of a dense network, which is represented here by their negative role in “$f_u$” term.
Figure 3. The variations of “f_iu” term at different levels of (a) “R” and “l” and (b) “t” and “u” parameters according to Equation (6).

Figure 4 illustrates the influences of “R” and “l” parameters on the electrical conductivity of PCNT predicted by the conventional and developed models in Equations (9) and (12). Figure 4a indicates that the least “R” and the high levels of “l” produce the highest conductivity. The “σ” level of 1100 S/m is observed at R = 10 nm and l > 6 μm. However, the conductivity significantly decreases at high and small levels of “R” and “l” parameters, respectively. Conclusively, the thinner and longer CNT produce a better conductivity in PCNT. Figure 4b also represents the similar trends between conductivity and these parameters based on the developed model, but the developed model predicts a higher level of conductivity at same levels of “R” and “l”.

The high values of radius and length of CNT cause negative and positive effects on the conductivity of nanocomposites. In general, the CNT significantly increase the poor conductivity of polymer matrix, which is in the range of 10^{-12} - 10^{-15} S/m. However, the thin and large CNT quicken the formation of filler network in PCNT, increase the effective volume fraction of CNT and also enhance the fraction of percolated CNT. So, the thin and long CNT, which occupy a large region of PCNT promptly produce a conductive network in PCNT at a very low percolation threshold and then, produce a big network in PCNT, which can effectively transport the electrons whole of PCNT and produce a significant electrical current. Therefore, the conduction efficiency of CNT in PCNT improves more by thinner and larger nanoparticles, as reported by the experimental measurements of electrical conductivity [62,63].

Figure 4. The roles of “R” and “l” parameters in the electrical conductivity of PCNT based on (a) conventional equation (Equation (9) at b = 2 and (b) developed model (Equation (12)).

Figure 5 reports the calculations of electrical conductivity at different levels of “t” and “u” parameters by the suggested models. Both models show the highest conductivity at the highest and the smallest levels of “t” and “u” factors, respectively. The conventional model (Figure 5a) calculates
the conductivity of 4000 S/m at \( t = 8 \) nm and \( u = 1 \), while conductivity decreases to about 0 at low levels of \( t^* \) and high values of \( u^* \). Moreover, Figure 5b based on the developed model demonstrates the highest conductivity as 7000 S/m at \( t = 8 \) nm and \( u = 1 \), while an insulated nanocomposite is approximately observed at the low and great values of \( t^* \) and \( u^* \) parameters, respectively. As a result, both models theoretically indicate that the conductivity more improves by thicker interphase and less waviness. On the other hand, the conductivity does not increase in PCNT containing thin interphase and waved CNT. In conclusion, the interphase thickness and the waviness of CNT directly and inversely affect the electrical conductivity of PCNT.

![Figure 5](image)

**Figure 5.** The electrical conductivity of PCNT at different \( t^* \) and \( u^* \) values according to (a) conventional model (\( b = 2 \), Equation (9)) and (b) developed equation (Equation (12)).

The high efficiencies of a thick interphase in percolation threshold, effective CNT and percolated nanotubes were mentioned. Now, it can be stated that the thick interphase supports the nanoparticles to form a conductive network at a low percolation. Furthermore, it is theoretically considered that a thick interphase pushes the nanotubes to form a big network in PCNT by connecting the interphase regions. All these phenomena promote the charge transfer in PCNT, which improves the electrical conductivity of PCNT. In fact, the formation of interphase layer around the nanoparticles as tunneling distance undoubtedly enhances the conducting efficiency of CNT in PCNT. Previous articles reported the tunneling conduction in the nanocomposites [64–66]. This phenomenon can be verified by plotting current vs. voltage in the nanocomposite, which exhibited a highly non-linear behavior [66].

Previously, the reinforcing effect of interphase regions in polymer nanocomposites was well reported in the articles [61,67]. In addition, \( u = 1 \) produces the highest conductivity in PCNT, because it demonstrates the straight CNT without waviness (Equation (2)). The negative role of waviness in the conductivity of PCNT is interpreted by its impact on the effective length and natural conductivity of CNT. The waved CNT produce a short length, which worsens the percolation threshold for network formation and the fraction of percolated nanoparticles, which both result in less effective CNT. These remarks indicate that the waviness of CNT postpones the formation of conductive structure in PCNT and also, decreases the size and density of network. Accordingly, experimental and theoretical data indicate that the waviness of CNT losses the effectiveness of the CNT network for electron transferring, which leads to a poor electrical conductivity in PCNT. On the other hand, the natural conductivity of CNT weakens by their waviness as illustrated in Equation (8). So, the networks of waved CNT show less conductivity compared to those containing straight nanotubes, which cannot significantly improve the electrical conductivity of insulate polymer matrices.

The effects of \( \phi_p \) and \( \phi_{eff} \) parameters on the conductivity of PCNT predicted by conventional model are depicted in Figure 6a. A low value of \( \phi_{eff} \) decreases the conductivity to about 0, but the smallest value of \( \phi_p \) and the highest level of \( \phi_{eff} \) produce the highest conductivity as 2500 S/m. Therefore, the least percolation threshold and the highest effective CNT
fraction increase the conductivity of PCNT. Moreover, Figure 6b demonstrates that the high levels of both “fiu” and “ϕeff” parameters positively improve the conductivity of PCNT based on the developed model. The conductivity of 7000 S/m is observed at fiu = 0.5 and ϕeff = 0.06, while the poor conductivity of about 700 S/m is estimated at fiu = 0.1 and ϕeff = 0.02. Therefore, the low value of “ϕp” as well as the great ranges of “fiu” and “ϕeff” parameters causes the high conductivity of PCNT.

![Graph](image)

Figure 6. The variations of electrical conductivity in PCNT by (a) various levels of “ϕp” and “ϕeff” parameters at b = 2 by conventional model (Equation (9)) and (b) different “fiu” and “ϕeff” ranges based on the developed model (Equation (12)).

The percolation threshold is the critical volume fraction of CNT in PCNT in which the conductive network forms. Accordingly, its low level produces the conductivity in PCNT at very low concentration of CNT. In addition, the helpful impact of low “ϕp” on “fiu” is understood from Equation (6), which suggests that a low percolation threshold produces a percolated network by a large number of CNT. According to these explanations, the promotion of conductivity by small percolation level is unavoidable. Moreover, a high level of “ϕeff” expresses that the CNT dimensions and interphase thickness produce more effective CNT, which considerably grows the electrical conductivity of PCNT. Furthermore, a great level of “fiu” shows the involvement of a large quantity of CNT in the percolated phase producing large and dense networks in PCNT, which can quickly transport the charge in PCNT. Accordingly, a higher “fiu” is representative of a bigger and denser network of CNT in PCNT, which significantly stimulates the electrical conductivity.

4. Conclusions

The effective volume fraction of CNT, percentages of percolated filler after percolation threshold and electrical conductivity in PCNT were expressed assuming the tunneling effect by interphase layer around nanoparticles. Thin and long CNT, thick interphase, and low waviness caused positive effects on the fraction of percolated CNT, but a high effective filler fraction was only obtained by thin CNT and thick interphase. Thin and long CNT caused a low distance among nanotubes in PCNT, which increased the probability of connection and networking. Also, a thick interphase showed a strong contribution to the connection of CNT, because it can push the separated nanotubes to form a conductive network. The waviness also decreased the effective length of nanotubes, which weakened their percolation and joining. According to these explanations, it was logical to obtain the highest conductivity of PCNT by the thinnest and the longest CNT, the thickest interphase, and the smallest waviness. These parameters effectively changed the effective properties of CNT and network; so, they significantly governed the electrical conductivity of PCNT. It was also reported that a low value of “ϕeff” did not change the conductivity of PCNT, but the smallest ϕp =
0.001 and the highest $\phi_{eff} = 0.06$ produced the highest conductivity of 2500 S/m by conventional model. Also, the highest conductivity of 7000 S/m was observed at the highest values of $f_w = 0.5$ and $\phi_{eff} = 0.06$ based on the developed model. These evidences demonstrated that the low value of “$\phi_p$” as well as the great ranges of both “$f_w$” and “$\phi_{eff}$” terms induced the high conductivity of PCNT.

**Author Contributions:** Conceptualization, Y.Z.; Methodology, Y.Z.; Software, Y.Z.; Validation, Y.Z. and K.Y.R.; Writing-Original Draft Preparation, Y.Z.; Writing-Review & Editing, Y.Z. and K.Y.R.; Supervision, K.Y.R.; Project Administration, K.Y.R.; Funding Acquisition, K.Y.R. All authors have read and agreed to the published version of the manuscript.

**Funding:** This research received no external funding

**Conflicts of Interest:** The authors declare no conflict of interest.

**References**

1. Zare, Y.; Rhee, K.Y. Prediction of loss factor (tan δ) for polymer nanocomposites as a function of yield tress, relaxation time and the width of transition region between Newtonian and power-law behaviors. *J. Mech. Behav. Biomed. Mater.* 2019, 96, 136–143.

2. Mittal, G.; Rhee, K.Y. Chemical vapor deposition-based grafting of CNTs onto basalt fabric and their reinforcement in epoxy-based composites. *Compos. Sci. Technol.* 2018, 165, 84–94.

3. Mittal, G.; Nešović, K.; Rhee, K.Y.; Mišković-Stanković, V. Investigation of corrosion behaviour of carbon nanotubes coated basalt fabric as a reinforcement material. *Compos. Part B Eng.* 2019, 178, 107493.

4. Tang, Z.; Jia, S.; Shi, X.; Li, B.; Zhou, C. Coaxial Printing of Silicone Elastomer Composite Fibers for Stretchable and Wearable Piezoresistive Sensors. *Polymers* 2019, 11, 666.

5. Liu, S.; Wu, G.; Chen, X.; Zhang, X.; Yu, J.; Liu, M.; Zhang, Y.; Wang, P. Degradation Behavior In Vitro of Carbon Nanotubes (CNTs)/Poly (lactic acid)(PLA) Composite Suture. *Polymers* 2019, 11, 1015.

6. Otaegi, I.; Aranburu, N.; Iturrondebeitia, M.; Ibarretxe, J.; Guerrica-Echevarría, G. The Effect of the Preparation Method and the Dispersion and Aspect Ratio of CNTs on the Mechanical and Electrical Properties of Bio-Based Polyamide-4, 10/CNT Nanocomposites. *Polymers* 2019, 11, 2059.

7. Wang, C.-F.; Wang, W.-N.; Lin, C.-H.; Lee, K.-I.; Hu, C.-C.; Lai, J.-Y. Facile Fabrication of Durable Superhydrophobic Films from Carbon Nanotube/Main-Chain Type Polybenzoxazine Composites. *Polymers* 2019, 11, 1183.

8. Wu, G.; Gu, Y.; Hou, X.; Li, R.; Ke, H.; Xiao, X. Hybrid Nanocomposites of Cellulose/Carbon-Nanotubes/Polyurethane with Rapidly Water Sensitive Shape Memory Effect and Strain Sensing Performance. *Polymers* 2019, 11, 1586.

9. Wang, J.; Cao, C.; Chen, X.; Ren, S.; Chen, Y.; Yu, D.; Chen, X. Orientation and Dispersion Evolution of Carbon Nanotubes in Ultra High Molecular Weight Polyethylene Composites under Extensional-Shear Coupled Flow: A Dissipative Particle Dynamics Study. *Polymers* 2019, 11, 154.

10. Keshtkar, M.; Mehdipour, N.; Eslami, H. Thermal Conductivity of Polyamide-6, 6/Carbon Nanotube Composites: Effects of Tube Diameter and Polymer Linkage between Tubes. *Polymers* 2019, 11, 1465.

11. Yue, Y.; Wang, X.; Wu, Q.; Han, J.; Jiang, J. Assembly of Polyacrylamide-Sodium Alginate-Based Organic-Inorganic Hydrogel with Mechanical and Adsorption Properties. *Polymers* 2019, 11, 1239.

12. Wang, X.; Wang, H.; Liu, B. Carbon Nanotube-Based Organic Thermoelectric Materials for Energy Harvesting. *Polymers* 2018, 10, 1196.

13. Zagho, M.; AlMaadeed, M.; Majeed, K. Thermal properties of TiO2NP/CNT/LDPE hybrid nanocomposite films. *Polymers* 2018, 10, 1270.

14. Kalkhoran, A.H.Z.; Naghib, S.M.; Vahidi, O.; Rahamian, M. Synthesis and characterization of graphene-grafted gelatin nanocomposite hydrogels as emerging drug delivery systems. *Biomed. Phys. Eng. Express* 2018, 4, 055017.

15. Naghib, S.M. Two dimensional functionalized methacrylated graphene oxide nanosheets as simple and inexpensive electrodes for biosensing applications. *Micro Nano Lett.* 2019, 14, 462–465.

16. Askari, E.; Naghib, S.M.; Seyfoori, A.; Maleki, A.; Rahamian, M. Ultrason-Assisted Synthesis and in Vitro Biological Assessments of a Novel Herceptin-Stabilized Graphene Using Three Dimensional Cell Spheroid. *Ultrason. Sonochem.* 2019, 58, 104615.
17. Zare, Y.; Rhee, K.Y. Modeling of viscosity and complex modulus for poly (lactic acid)/poly (ethylene oxide)/carbon nanotubes nanocomposites assuming yield stress and network breaking time. Compos. Part B Eng. 2019, 156, 100–107.

18. Zare, Y.; Rhee, K.Y. Following the morphological and thermal properties of PLA/PEO blends containing carbon nanotubes (CNTs) during hydrolytic degradation. Compos. Part B Eng. 2019, 175, 107132.

19. Salabandish, R.; Ghaffarinejad, A.; Naghib, S.M.; Majidzadeh-A, K.; Sanati-Nezhad, A. A novel graphene-grafted gold nanoparticles composite for highly sensitive electrochemical biosensing. IEEE Sens. J. 2018, 18, 2513–2519.

20. Naghib, S.M.; Parnian, E.; Keshviri, H.; Omidinia, E.; Eshghan-Malek, M. Synthesis, characterization and electrochemical evaluation of polyvinylalcohol/graphene oxide/silica nanocomposites for glucose biosensing application. Int. J. Electrochem. Sci. 2018, 13, 1013–1026.

21. Rostami, A.; Vahdati, M.; Nazockdast, H. Unraveling the localization behavior of MWCNTs in binary polymer blends using thermodynamics and viscoelastic approaches. Polym. Compos. 2018, 39, 2356–2367.

22. Rostami, A.; Eskandari, F.; Masoomi, M.; Nowrouzi, M. Evolution of Microstructure and Physical Properties of PMMA/MWCNTs Nanocomposites upon the Addition of Organoclay. J. Oil Gas Petrochem. Technol. 2019, 6, 28–38.

23. Kim, S.; Zare, Y.; Garmabi, H.; Rhee, K.Y. Variations of tunneling properties in poly (lactic acid)/(PLA/poly (ethylene oxide)/(PEO)/carbon nanotubes (CNT) nanocomposites during hydrolytic degradation. Sens. Actuators A Phys. 2018, 274, 28–36.

24. Zare, Y.; Park, S.P.; Rhee, K.Y. Analysis of complex viscosity and shear thinning behavior in poly (lactic acid)/poly (ethylene oxide)/carbon nanotubes biosensor based on Carreau–Yasuda model. Results Phys. 2019, 13, 10245.

25. Naghib, S.M. Fabrication of Nanofiber/Silver Nanoparticles/Reduced Graphene Nanosheets/Glucose Oxidase Nanobiocomposite for Electrochemical Glucose Biosensing. Anal. Bioanal. Electrochim. 2016, 8, 453–465.

26. Zare, Y.; Rhee, K.Y.; Park, S.J. Simple model for hydrolytic degradation of (lactic acid)/poly (ethylene oxide)/carbon nanotubes nanosensor in neutral phosphate-buffered saline solution. J. Biomed. Mater. Res. Part. A 2019, 107, 2706–2717.

27. Mamaghani, K.R.; Naghib, S.M.; Zahedi, A.; Kalkhoran, A.H.Z.; Rahmanian, M. Fast synthesis of methacrylated graphene oxide: A graphene-functionalised nanostructure. Micro Nano Lett. 2018, 13, 195–197.

28. Martins, J.N.; Bassani, T.S.; Barra, G.M.; Oliveira, R.V. Electrical and rheological percolation in poly (vinylidene fluoride)/multi-walled carbon nanotube nanocomposites. Polym. Int. 2011, 60, 430–435.

29. Maiti, S.; Shrivastava, N.K.; Khatau, B. Reduction of percolation threshold through double percolation in melt-blended polycarbonate/acylonitrile butadiene styrene/multiwall carbon nanotubes elastomer nanocomposites. Polym. Compos. 2013, 34, 570–579.

30. Clingerman, M.L.; King, J.A.; Schulz, K.H.; Meyers, J.D. Evaluation of electrical conductivity models for conductive polymer composites. J. Appl. Polym. Sci. 2002, 83, 1341–1356.

31. Zare, Y.; Rhee, K.Y. Evaluation of the Tensile Strength in Carbon Nanotube-Reinforced Nanocomposites Using the Expanded Takayanagi Model. JOM 2019, 71, 3980–3988.

32. Esbati, A.; Irani, S. Effect of functionalized process and CNTs aggregation on fracture mechanism and mechanical properties of polymer nanocomposite. Mech. Mater. 2018, 118, 106–119.

33. Combessis, A.; Bayon, L.; Flandin, L. Effect of filler auto-assembly on percolation transition in carbon nanotube/polymer composites. Appl. Phys. Lett. 2013, 102, 011907.

34. Chang, L.; Friedrich, K.; Ye, L.; Toro, P. Evaluation and visualization of the percolating networks in multi-wall carbon nanotube/epoxy composites. J. Mater. Sci. 2009, 44, 4003–4012.

35. Kara, S.; Arda, E.; Dolastir, F.; Pekcan, O. Electrical and optical percolations of polystyrene latex–multiwalled carbon nanotube composites. J. Colloid Interface Sci. 2010, 344, 395–401.

36. Ma, H.; Gao, X.-L. A three-dimensional Monte Carlo model for electrically conductive polymer matrix composites filled with curved fibers. Polymer 2008, 49, 4230–4238.

37. Zare, Y.; Rhim, S.; Garmabi, H.; Rhee, K.Y. A simple model for constant storage modulus of poly (lactic acid)/poly (ethylene oxide)/carbon nanotubes nanocomposites at low frequencies assuming the properties of interphase regions and networks. J. Mech. Behav. Biomed. Mater. 2018, 80, 164–170.

38. Zare, Y.; Rhee, K.Y.; Park, S.-J. A modeling methodology to investigate the effect of interfacial adhesion on the yield strength of MMT reinforced nanocomposites. J. Ind. Eng. Chem. 2019, 69, 331–337.
39. Zare, Y.; Rhee, K.Y. Tensile strength prediction of carbon nanotube reinforced composites by expansion of cross-orthogonal skeleton structure. Compos. Part B Eng. 2019, 161, 601–607.

40. Zare, Y.; Rhee, K.Y. Effects of interphase regions and filler networks on the viscosity of PLA/PEO/carbon nanotubes biosensor. Polym. Compos. 2019, 40, 4135–4141.

41. Mortazavi, B.; Bardon, J.; Ahzi, S. Interphase effect on the elastic and thermal conductivity response of polymer nanocomposite materials: 3D finite element study. Comput. Mater. Sci. 2013, 69, 100–106.

42. Montazeri, A.; Naghdabadi, R. Investigation of the interphase effects on the mechanical behavior of carbon nanotube polymer composites by multiscale modeling. J. Appl. Polym. Sci. 2010, 117, 361–367.

43. Celzard, A.; McRae, E.; Deleuze, C.; Dufort, M.; Furdin, G.; Maréché, J. Critical concentration in percolating systems containing a high-aspect-ratio filler. Phys. Rev. B 1996, 53, 6209.

44. Qiao, R.; Brinson, L.C. Simulation of interphase percolation and gradients in polymer nanocomposites. Compos. Sci. Technol. 2009, 69, 491–499.

45. Lu, P.; Leong, Y.; Pallathadka, P.; He, C. Effective moduli of nanoparticle reinforced composites considering interphase effect by extended double-inclusion model–Theory and explicit expressions. Int. J. Eng. Sci. 2013, 73, 33–55.

46. Shin, H.; Yang, S.; Choi, J.; Chang, S.; Cho, M. Effect of interphase percolation on mechanical behavior of nanoparticle-reinforced polymer nanocomposite with filler agglomeration: A multiscale approach. Chem. Phys. Lett. 2015, 635, 80–85.

47. Razavi, R.; Zare, Y.; Rhee, K.Y. The roles of interphase and filler dimensions in the properties of tunneling spaces between CNT in polymer nanocomposites. Polym. Compos. 2019, 40, 801–810.

48. Baxter, S.C.; Robinson, C.T. Pseudo-percolation: Critical volume fractions and mechanical percolation in polymer nanocomposites. Compos. Sci. Technol. 2011, 71, 1273–1279.

49. Du, F.; Scogna, R.C.; Zhou, W.; Brand, S.; Fischer, J.E.; Winey, K.I. Nanotube networks in polymer nanocomposites: Rheology and electrical conductivity. Macromolecules 2004, 37, 9048–9055.

50. Takeda, T.; Shindo, Y.; Kunouma, Y.; Narita, F. Modeling and characterization of the electrical conductivity of carbon nanotube-based polymer composites. Polymer 2011, 52, 3852–3856.

51. Deng, F.; Zheng, Q.-S. An analytical model of effective electrical conductivity of carbon nanotube composites. Appl. Phys. Lett. 2008, 92, 071902.

52. Zare, Y.; Rhee, K.Y.; Park, S.-J. A developed equation for electrical conductivity of polymer carbon nanotubes (CNT) nanocomposites based on Halpin-Tsai model. Results Phys. 2019, 14, 102406.

53. Zare, Y.; Rhee, K.Y.; Park, S.-J. Modeling the roles of carbon nanotubes and interphase dimensions in the conductivity of nanocomposites. Results Phys. 2019, 15, 102562.

54. Zare, Y.; Rhee, K.Y. A multistep methodology for effective conductivity of carbon nanotubes reinforced nanocomposites. J. Alloy. Compd. 2019, 793, 1–8.

55. Kim, Y.J.; Shin, T.S.; Do Choi, H.; Kwon, J.H.; Chung, Y.-C.; Yoon, H.G. Electrical conductivity of chemically modified multiwalled carbon nanotube/epoxy composites. Carbon 2005, 43, 23–30.

56. Zare, Y.; Rhee, K.Y. The effective conductivity of polymer carbon nanotubes (CNT) nanocomposites. J. Phys. Chem. Solids 2019, 131, 15–21.

57. Zare, Y.; Rhee, K.Y. A Simulation Work for the Influences of Aggregation/Agglomeration of Clay Layers on the Tensile Properties of Nanocomposites. JOM 2019, 71, 3989–3995.

58. Lisunova, M.; Mamunya, Y.P.; Lebovka, N.; Melezhhyk, A. Percolation behaviour of ultrahigh molecular weight polyethylene/multi-walled carbon nanotubes composites. Eur. Polym. J. 2007, 43, 949–958.

59. Sevostianov, I.; Kachanov, M. Effect of interphase layers on the overall elastic and conductive properties of matrix composites. Applications to nanosize inclusion. Int. J. Solids Struct. 2007, 44, 1304–1315.

60. Joshi, P.; Upadhyay, S. Effect of interphase on elastic behavior of multiwalled carbon nanotube reinforced composite. Comput. Mater. Sci. 2014, 87, 267–273.

61. Zare, Y.; Rhee, K.Y. A multistep methodology for calculation of the tensile modulus in polymer/carbon nanotube nanocomposites above the percolation threshold based on the modified rule of mixtures. RSC Adv. 2018, 8, 30986–30993.

62. Arenhart, R.; Barra, G.; Fernandes, C. Simulation of percolation threshold and electrical conductivity in composites filled with conductive particles: Effect of polydisperse particle size distribution. Polym. Compos. 2016, 37, 61–69.

63. Berhan, L.; Sastry, A. Modeling percolation in high-aspect-ratio fiber systems. I. Soft-core versus hard-core models. Phys. Rev. E 2007, 75, 041120.
64. Celzard, A.; Furdin, G.; Mareche, J.; McRae, E. Non-linear current-voltage characteristics in anisotropic epoxy resin-graphite flake composites. *J. Mater. Sci.* 1997, 32, 1849–1853.

65. Paredes-Madrid, L.; Palacio, C.; Matute, A.; Parra Vargas, C. Underlying physics of conductive polymer composites and force sensing resistors (FSRs) under static loading conditions. *Sensors* 2017, 17, 2108.

66. Koke, S.; Grebing, C.; Frei, H.; Anderson, A.; Assion, A.; Steinmeyer, G. Direct frequency comb synthesis with arbitrary offset and shot-noise-limited phase noise. *Nat. Photonics* 2010, 4, 462.

67. Chen, S.; Sarafbidabad, M.; Zare, Y.; Rhee, K.Y. Estimation of the tensile modulus of polymer carbon nanotube nanocomposites containing filler networks and interphase regions by development of the Kolarik model. *RSC Adv.* 2018, 8, 23825–23834.

© 2020 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/).