Prediction of Propeller Performance using Computational Fluid Dynamics Approach

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Abstract

A reliable prediction approach to obtain a sufficient thrust and torque to propel the ship at desired forward speed is obviously required. To achieve this objective, the authors propose to predict the thrust coefficient (K1), torque coefficient (K0) and efficiency (Ƞ) of the propeller in open-water model test condition using Computational Fluid Dynamics (CFD) simulation approach. The computational simulation presented in the various number of rotational speed (RPM) within the range of advance ratio J=0.1 up to 1.05. The higher value of J leads to a decrease in 10K0 and K1. While the η increased steadily at the lower value of J and decreased at the higher value of J. The results also showed that the propeller with 1048 rpm obtains a better efficiency at J=0.95 with η= 88.25%, 10K0=0.1654 and K1= 0.0942. The computation result is very useful as preliminary data for propeller performance characteristics.

Keywords: CFD; efficiency; propeller; RPM; thrust

1. Introduction

The main purpose of a marine propeller to deliver the power and torque provided by the engine into the rotational motion to generate thrust. A proper specification of propeller design is required to make sure the propeller can produce a driving force to move the ship forward in the most effective ways [1, 2]. Other than that, improper propeller design and specification have a direct influence on the reduction of propeller performance and fuel efficiency of the ship propulsion system [3, 4]. The configuration of the propeller becomes a typical discussion among the naval architectures because the selection of the proper propeller design depends on the specification of the vessel and it also affects the manufacturing cost. Therefore, a hydrodynamics characteristic of the propeller is a very prominent aspect to be analysed in the early design stage using several methods in the form of open-water propeller model test.

Several researchers have been investigating the hydrodynamics characteristics of propeller using numerical and experimental approaches. According to [5-8], mathematical methods can be used to predict the hydrodynamics characteristics of the propeller based on circulation or lifting line theory. Meanwhile, hydrodynamics characteristics of the propeller are also predicted by using an experimental model test with towing tank [9-11]. This experimental method is very expensive, time-consuming, and have a complex procedure for various hydrodynamics analysis test configuration. Following the works of [12-16], the numerical methods are adopted to solve and analyze the fluid problem. The computational fluid dynamics (CFD) simulation are the best alternative with several advantages such as allow to simulate using actual and model geometry scale in extreme condition of the fluid flow and the CFD simulation also have a good agreement with experimental data [17-20].

This paper presents a CFD simulation approach for the extension work from [21, 22] to access the performance of propeller by K1, K0, and η of the propeller. Here, a commercial CFD software, namely NUMECA FineTM/Turbo v12.2 is utilized by grid generation, flow solver and post-processing capabilities. FineTM/Turbo is specialized to simulate internal, rotating and turbomachinery flows for all types of fluids. The package has a fully hexahedral and highly automated grid generation module
AutoGrid™. The package uses a 3D Reynolds Averaged Euler and Navier Stokes flow solver EURANUS. CFView™ is a post-processing module which is also part of the package. Basically, this is solved by means of a grid-independent study to estimate the optimal domain discretization. In this computation simulation, several numbers of rotational speed (rpm) are considered. The result is then comprehensively discussed to analyze their effect on Kt, Ko, and η with the purpose of quantifying propeller performance quality.

2. Methods and Material

2.1. Governing equation

The cornerstone of computational fluid dynamics application, there is consists of fundamental governing mathematical statements of fluid dynamics such as continuity, momentum, and energy conservation equation. The 3-D propeller simulation defines that the flow around the propeller is complex, due to the combination between rotation and progression into the water [3]. Therefore, the CFD flow solver (ISIS-CFD) on NUMECA Fine™/Turbo V12.2 was based on the incompressible unsteady Reynolds-Averaged Navier-Stokes equation (URANSE) in which the solver applied the Finite Volume Method for representing the inflow and outflow areas, where the fluid flow is well behaved. Here, the governing equation has been discriminated using a Finite Volume Method with the velocity-pressure coupling and operated using a SIMPLE algorithm [23]. The Finite Volume Method also able to directly apply the integral spatial discretization in the physical space coordinate transformation to a computational space and this method also flexible to complex geometry structured and unstructured meshes.

2.2. Governing equation

To carry out the application of general conservation form of the Navier-Stokes equation using Finite Volume Method, the model of a finite volume has been considered fixed in space and the fluid element is moving. The continuity equation in conservation form presented in Eq. (1), where the ρ= density, Ut is the averaged Cartesian components of the velocity-vector in i th direction (i=1,2,3). Since the propeller simulated in steady and constant density of incompressible flows, the continuity equation has been modified as Eq. 2 [11].

\[
\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i) = 0
\]

\[
\frac{\partial}{\partial t} (\rho u_i) = 0
\]

Newton’s 2nd law has been applied in Finite Volume Method to a model of the fluid flow. When the fluid element moving, the net force on the fluid element equals its mass times the acceleration of the element. Therefore, the global Navier-Stokes equation applied the principle of the linear momentum conservation to solve the problem. Here, the momentum conservation equation expressed as Eq. 3.

\[
\frac{\partial}{\partial t} (\rho u_i) + \frac{\partial}{\partial x_j} (\rho u_i u_j) = \frac{\partial}{\partial x_j} \left( \rho \frac{\partial u_i}{\partial x_j} \right) + F_i
\]

\[
\tau_{ij} = \left( \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \mu \frac{\partial}{\partial x_j} \delta_{ij} \right)
\]

where \( p \) = static pressure, \( g_i \) = gravitational acceleration, \( F_i \) = external body force in an averaged Cartesian component of the velocity-vector in i th direction (i=1,2,3) and \( \delta_{ij} \) = Kroneker delta and is equal to unity \( i = j \) and zero when \( i \neq j \) [12]. Finally, \( \tau_{ij} \) defined Reynolds-stress tensor presented below as Eq. 4, where \( \mu \) being the dynamics viscosity [3].

2.3. Turbulent model

During the simulation, a simple one-equation model has relatively applied to compute rotating motions of propeller. Deck [24], Kostic [25], Hejlesen [26] and Lorin [27], reported that the Spalart-Allmaras transports equation model made for eddy viscosity and not required finer grid resolution to capture the velocity field gradients with algebraic models. For internal flow (turbomachinery) application, the kinematic turbulent \( \nu = (m/s) \) in this model can be specified and estimate based on the assumptions, \( \frac{V_f}{V} = 1 \) to 5 [28]. Here, the transport model for the working variable is shown in Eq. 5:

\[
\frac{\partial \rho \nu}{\partial t} + \frac{\partial}{\partial x_j} (\rho \nu u_j) = \frac{\partial}{\partial x_j} \left( \left( \mu + \frac{\mu_t}{\sigma} \right) \frac{\partial \nu}{\partial x_j} \right) + c_{b2} \frac{\partial \nu}{\partial x_j} + c_{b1} \rho \nu \frac{\partial \nu}{\partial x_j} - c_{w1} f_{w1} \rho \left( \frac{\nu}{y} \right)
\]

The eddy viscosity and damping function are defined as Eqs. 6 and 7, respectively. Where, \( \chi = \frac{\nu}{y} \) and the kinematic viscosity \( \nu = \frac{\mu}{\rho} \).

\[
\mu_t = f_{i1} \rho \nu
\]

\[
f_{i1} = \frac{X^3}{X^3 + c_{i1}^3}
\]
It should be noted here that the best practice in turbulence modeling quantities by considering an appropriate grid to estimate the cell meshing size, $y_{wall}$. Referring to the transport model discussed above, the viscosity has been taken into account that presents the high gradients near solid wall layers. Therefore, it is very important to have a sufficient amount the number of grid points in the boundary layers to properly capture the high gradient [21]. Here, an appropriate estimation of cell meshing size, $y_{wall}$ for Navier-Stokes simulation, depends on the wall variable $y^+$ to measure the viscosity effect region as written in Eq. (8) [29].

$$y^+_w = \frac{\rho u^+_w y_{wall}}{\mu}$$  \hspace{1cm} (8)

where $u_w$ is the friction velocity, $u_w = \frac{\tau_{wall}}{\rho} = \frac{1}{2} \left( \frac{V_{ref}}{\nu} \right)^2 C_s$.

It is clear that the value of $y_{wall}$ depends on the value of $y^+_w$.

In addition, the estimation for $y_{wall}$ as a function of the desired value is obtained using a truncated series solution of the Blasius equation as expressed in Eq. (9).

$$y_{wall} = 6 \left( \frac{V_{ref}}{v} \right)^{\frac{2}{5}} \left( \frac{L_{ref}}{2} \right)^{\frac{1}{5}} y^+_w$$  \hspace{1cm} (9)

Note that the reference velocity, $V_{ref}$, can be taken from the body velocity. The reference length, $L_{ref}$, should be based on the body length since an estimation of the boundary layer thickness is implied in this calculation. For instance, in the case of a propeller simulation, one could use the propeller diameter, as reference length. This is approximate, of course, as the thickness of the boundary layer will vary widely within the computational domain. Fortunately, it is only necessary to place within a range and not at a specific value.

2.4. Hydrodynamics theory of propeller

In CFD computation, the rotational surface is utilized to compute the force and torque of the system, where the axial thrust projected by the global force on the rotational axis and the torque was exerted by the global force calculated at (0,0,0). Nevertheless, these quantities are computed from the pressure and the velocity fields of the fluid acting on the blade surfaces. The axial thrust is computed based on Eq. 12 [28];

$$\sum F \cdot \hat{n}_z$$  \hspace{1cm} (10)

The projection of the torque along a given direction $\hat{z}$ is given by

$$\left[ \sum \vec{r} \times \vec{F} \right] \cdot \hat{z}$$  \hspace{1cm} (11)

The propeller model has been tested in open water test to determine the intrinsic propeller performance without distributed by the ship when it moved forward. The computed result from CFD usually refers to thrust ($T$), torque ($Q$) and efficiency ($\eta$). Thus, the performance data are given as form dimensionless thrust coefficient ($K_T$) and torque coefficient ($K_Q$) to be plotted against the advance ratio ($J$). The dimensionless quantities are defined as

$$J = \frac{V_a}{n \cdot D}$$  \hspace{1cm} (12)

$$K_T = \frac{T}{\rho n^2 D^4}$$  \hspace{1cm} (13)

$$K_Q = \frac{Q}{\rho n^2 D^5}$$  \hspace{1cm} (14)

$$\eta = \frac{J}{K_T} \frac{K_Q}{2 \pi K_0}$$  \hspace{1cm} (15)

where $\rho$ is the water density, $n$ the number of propeller rotations per second (RPS), $D$ the propeller diameter and $V_a$ represents for water advance velocity ($m/s$).

3. Simulation Condition

3.1. Hydrodynamics theory of propeller

In this paper, different rotational speeds were used to investigate. The principal dimension of the propeller, which composes with four number of blades is clearly presented in Table 1 and Fig. 1.

| Geometrical parameters | Full Scale | Model Scale |
|------------------------|------------|-------------|
| Diameter (mm)          | 3650       | 119.25      |
| AE/AO                  | 0.695      | 0.695       |
| P/D                    | 1.013      | 1.013       |
| Pitch (mm)             | 3697.45    | 120.83      |
| Scale                  | 1:30.6     |             |
| Propeller Orientation  | Right-hand rotation |

Figure 1. 3D view of propeller geometry
3.2. Simulation condition

In this study, there are parametric studies to be focused to achieve the objectives. The parametric studies were based on Table 2.

3.3. Computational domain and grid generation

The numerical simulation of propeller performance in various configurations was developed from the commercial software NUMECA Fine™/Turbo. Here, a single propeller blades geometry needs to define the trailing edge, leading edge, pressure side, suction side, and the hub of the propeller to generate an automatic grid. This simulation only considered a single blade of the propeller and another blades are performed by using a rotational periodicity (number of blades) which is the block of the blades and boundary are repeated in a given axis by a specified angle to save the computational time (for all simulation condition) [30].

![Figure 2. 3D surface mesh for single blade associated with Z=4 mesh model](image)

![Figure 3. Local refinement of the block structured grid in Blade-to-Blade view](image)

![Figure 4. Upstream and downstream location in the domain](image)

![Figure 5. Upstream and downstream location in the domain](image)

Referring to Figure 4, the far-field boundary extends radially at five times (5R) the rear rotor radius at rotation center, while the axial length was located at three times radius (3R) for inlet and outlet boundary from the center as well. The inlet was specified as having a constant velocity of the flow model and a static pressure has been imposed at outlet boundary as shown in Fig. 5.

![Figure 6. Scalar torque contour for (a) pressure and (b) suction side at J=0.1 with 1048 RPM](image)

### Table 2. The simulation conditions

| Rotational Speed (RPM) | Number of blades (Z) |
|------------------------|----------------------|
| 1048                   | 4                    |
| 1200                   |                      |
| 1340                   |                      |

### Table 3. Mesh Independent study on propeller geometry

| Case | Total Number of Cell Meshing | $K_T$ | $10K_T$ | $\eta$ |
|------|-----------------------------|-------|---------|--------|
| A    | 1,789,042                   | 0.3679| 0.5541  | 0.1057 |
| B    | 2,559,546                   | 0.3719| 0.5563  | 0.1064 |
| C    | 2,817,090                   | 0.3727| 0.5571  | 0.1065 |
| D    | 4,000,666                   | 0.3744| 0.5551  | 0.1073 |
The value for the rotational speed of the solid boundary condition types (blades and hub) was set as a positive value to indicate a propeller rotation in positive θ-direction according to a right-handed propeller orientation [28]. Since this computational have a complex fluid problem, the Merkle preconditioner has been selected to increase the convergence rate and computation efficiency at very low flow speed [32, 30]. Besides, to overcome an insufficient calculation due to low relative edge cell size, a double solver precision has been selected to solve this computation and has led to increasing the required memory. The average duration of every simulation was about 4 to 7 hours (double solver precision) on a HP Z820 Workstation PC with processor Intel® Xeon® CPU ES-2690 v2 @ 3.0GHz (2 processor) associated with the installed memory RAM of 32.0 GB and 64-bit operating system.

The meshing generation of the propeller was created in AutoGrid5 v12.2 software. It should note that an adequate number of mesh is very important for proper and accurate simulation. Hence, a mesh independent study may need to be performed for four different total number of cell meshing. Referring to mesh independent study result, the case C with 2.8 million total number of cell meshing was selected in all computed simulation of the propeller model accuracy of the CFD solution. This can be explained by the fact the 4.0 million total number of cell meshing were unnecessary due to its insignificant influence on the computational result of the thrust coefficient, torque coefficient, and efficiency. In the final stage of the CFD simulation, a package software in CFView was used to visualize the scalar torque for pressure and suction side for all various configurations of the propeller as displayed in Fig. 6.

4. Results and Discussions

The analysis for thrust coefficient, torque coefficient, and efficiency of the propeller in various rotational speed (RPM) was analyzed in the steady-state have been presented and appropriately discussed. In this study, the Computational Fluid Dynamics (CFD) approach was utilized to obtain the propeller performance.

Figure 7. Thrust coefficient, torque coefficient, and efficiency for 1048 RPM

4.1. Propeller performance in various rotational speed

Referring to the Fig. 7, the $K_T$ and $10K_Q$ decreases by increasing the advance ratio, $J$. Besides, the $\eta$ increase steadily at lower advance ratio ($J = 0.10$) up to propeller optimum value ($J = 0.95$) and decreased at higher advance ratio ($J = 1.00$ and 1.05) as showed in Fig. 7 and detailed value in Table 4. The effect to the $K_T$ occurs due to low axial velocity, the water surrounding the propeller will be accelerated from a low velocity. While at the higher advance ratio, the water surrounds the propeller already moving at high velocity and makes less change to the water velocity [33]. Besides that, the effect of $10K_Q$ due to the decreasing drag force on the blade surface. According to [33], the water pressure surrounding the blade was high when the water condition at a low velocity and directly contributes to pressure drag on the blade surface. While at high water velocity, the water pressure surrounding the blades will drop slowly and the pressure drag also drops as shown in Figure 8. This can be explained by the fact that the lowest pressure drags at leading edge (light blue color) resulted in lower scalar torque value as presented in Fig. 9.

The result of testing the propeller model on the various rotational speed of 1048, 1200 and 1340 RPM are represented in Fig. 10. The results showed that the $10K_Q$, $K_T$ and $\eta$ value obviously had a similar trend with the results at 1048 rpm from $J=0.10$ up to 1.05. Generally, the comparison between these three numbers of rpm shows that increasing the rpm results in decreasing $10K_Q$, $K_T$ and $\eta$ of the propeller. The propeller optimum, for 1048 rpm at about $J=0.95$ was achieved at $\eta=88.25\%$ with $10K_Q=0.1614$ and $K_T=0.0942$. Besides, the optimum efficiency of the propeller for 1200 RPM occurs at $J=0.90$ with $\eta=73.93\%$, $10K_Q=0.2318$, and $K_T=0.1021$. While, the optimum J value for 1340 rpm at about $J=0.85$ with 67.41$, 10K_Q=0.2318$, and $K_T = 0.1298$. As compared with various rotational speeds, the propeller with 1048 RPM obtains better efficiency that can be explained by the fact that the propeller with low RPM will absorb less power to achieve requested RPM. According to [34] and [35], the propeller rotation speed greatly influences the blades pressure distribution where the higher rpm resulting in the lower pressure at the
blade surface; where blue color indicates low pressure area increase as higher propeller revolution (see Fig. 11). Meanwhile, the negative pressure magnitude direction being against the propeller continued to increase and expand in the back region. In this situation, the hydrodynamics performance of the 1340 RPM shows that the propeller with high rpm will produce lower pressure at suction side.

![Figure 10. Thrust coefficient, torque coefficient, and efficiency for various rotational speeds](image)

Table 4. Thrust coefficient, torque coefficient, and efficiency for various rotational speeds

| J   | 1048 RPM | 1200 RPM | 1340 RPM |
|-----|----------|----------|----------|
|     | K₀       | Kₜ       | η         | K₀       | Kₜ       | η         | K₀       | Kₜ       | η         |
| 0.10| 0.5562   | 0.3892   | 0.1114    | 0.5571   | 0.3727   | 0.1065    | 0.5505   | 0.3573   | 0.1033    |
| 0.15| 0.5545   | 0.3873   | 0.1668    | 0.5464   | 0.3638   | 0.1590    | 0.5401   | 0.3488   | 0.1542    |
| 0.20| 0.5367   | 0.3725   | 0.2209    | 0.5355   | 0.3546   | 0.2108    | 0.5296   | 0.3399   | 0.2043    |
| 0.25| 0.5258   | 0.3630   | 0.2747    | 0.5238   | 0.3445   | 0.2617    | 0.5184   | 0.3303   | 0.2535    |
| 0.30| 0.5137   | 0.3524   | 0.3276    | 0.5109   | 0.3334   | 0.3116    | 0.5061   | 0.3197   | 0.3016    |
| 0.35| 0.4993   | 0.3401   | 0.3794    | 0.4968   | 0.3213   | 0.3603    | 0.4949   | 0.3100   | 0.3490    |
| 0.40| 0.4846   | 0.3277   | 0.4305    | 0.4808   | 0.3079   | 0.4077    | 0.4768   | 0.2948   | 0.3936    |
| 0.45| 0.4684   | 0.3141   | 0.4802    | 0.4628   | 0.2930   | 0.4534    | 0.4593   | 0.2802   | 0.4370    |
| 0.50| 0.4464   | 0.2967   | 0.5288    | 0.4425   | 0.2766   | 0.4974    | 0.4391   | 0.2639   | 0.4782    |
| 0.55| 0.4206   | 0.2781   | 0.5788    | 0.4174   | 0.2583   | 0.5416    | 0.4144   | 0.2455   | 0.5187    |
| 0.60| 0.3936   | 0.2588   | 0.6278    | 0.3903   | 0.2389   | 0.5845    | 0.3866   | 0.2258   | 0.5577    |
| 0.65| 0.3654   | 0.2385   | 0.6752    | 0.3619   | 0.2186   | 0.6248    | 0.3590   | 0.2061   | 0.5938    |
| 0.70| 0.3359   | 0.2173   | 0.7206    | 0.3325   | 0.1975   | 0.6616    | 0.3296   | 0.1850   | 0.6254    |
| 0.75| 0.3049   | 0.1950   | 0.7635    | 0.3017   | 0.1754   | 0.6940    | 0.2986   | 0.1629   | 0.6510    |
| 0.80| 0.2722   | 0.1717   | 0.8031    | 0.2691   | 0.1522   | 0.7201    | 0.2662   | 0.1398   | 0.6686    |
| 0.85| 0.2376   | 0.1472   | 0.8383    | 0.2344   | 0.1277   | 0.7368    | 0.2318   | 0.1155   | 0.6741    |
| 0.90| 0.2009   | 0.1215   | 0.8665    | 0.1978   | 0.1021   | 0.7393    | 0.1952   | 0.0900   | 0.6602    |
| 0.95| 0.1614   | 0.0942   | 0.8825    | 0.1587   | 0.0751   | 0.7155    | 0.1560   | 0.0629   | 0.6099    |
| 1.00| 0.1196   | 0.0656   | 0.8735    | 0.1168   | 0.0465   | 0.6336    | 0.1144   | 0.0346   | 0.4813    |
| 1.05| 0.0750   | 0.3892   | 0.7917    | 0.0722   | 0.0165   | 0.3822    | 0.0698   | 0.0047   | 0.1117    |
Figure 11. 2D static pressure contour for various rotational speed

Figure 12. Scalar torque contour at pressure side for various rotational speed
5. Conclusion

The Computational Fluid Dynamics (CFD) simulation on hydrodynamic analysis of propeller is performed using NUMECA Fine™/Turbo v.12.2 software. The analysis of propeller performance was summarized as follow:

- The higher value of J lead to decrease 10K₀, Kᵣ, and η due to low axial velocity and pressure drag surrounding the propeller.
- The increasing number of rotational speed (RPM), will decrease the propeller performance (10K₀, Kᵣ and η).
- As compared with various numbers of rpm, the optimum efficiency of the propeller with 1048 RPM at J = 0.95 with η = 88.25%, 10K₀ = 0.1614 and Kᵣ = 0.0942 produce a better efficiency.

In general, the effect of various rotational speeds has a positive influence on the open water characteristics of the marine propeller. Therefore, these CFD results are useful as a preliminary prediction of propeller performance.

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