Harmonic spectra of BLDC motor supplied by a solar PV

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ABSTRACT
The multilevel inverters have been used especially in renewable energy aspects in order to assess total harmonic distortion (THD). THD is considered to produce a good quality of current signal of BLDC motor drive. In this paper, a solar PV inverter fed brushless DC (BLDC) motor drive is discussed considering two topologies of three phase multilevel inverters. These topologies are flying capacitor and clamped diode inverters. The inverter efficiency and output power have an effectiveness on THD values. A boost dc to dc converter using incremental conductance maximum power point tracking (INC-MPPT) is implemented with a solar PV. The mathematical model of the proposed systems are studied via simulation using Matlab/Simulink. The simulation results of a BLDC motor based on two multilevel inverters are compared with each other considering the THD and the utilization of the dc-bus voltage, the comparison verified that the clamped diode inverter has a better harmonic spectra still the overshoot is a little bit high in the two types of inverter that are proposed.

Keywords:
BLDC motor
Harmonic distortion
Multilevel inverter
Space-vector modulation

1. INTRODUCTION
The motivation of increasing use of BLDC motor in many applications such as: computer hard disk drives, military and industrial. This is due to an improvement of permanent magnet construction as well as the improvement of the power electronic devices. Moreover, the motor design cost is rapidly decreasing. Therefore, it has been illustrated that in the past few years the BLDC motors are utilized in different applications starting from the simple ones like pumps or fans to high performance drives like machine-tools servos and applications that require high level of speed regulation like hybrid electric vehicles. This is all because this type of motors contains special features such as high torque to inertia ratio, high reliability, low cost, and high power per weight ratio [1].

Recently multilevel inverters have been used especially in renewable energy aspects in order to assess THD [2-5]. Two topologies of three-phase inverter are tested and implemented with BLDC motor drive. These topologies are the flying capacitor inverter and clamped diode inverter [6-7]. Amol K. Koshti, M. N. Rao (2017) [8] discussed the different multilevel inverter (MLI) topologies review including diode clamped multilevel DC-MLI) inverter, flying capacitor multilevel FC-MLI) inverter, cascaded H-bridge (CHB) converter and it introduced their applications in renewable energy [9-11].

A space vector pwm (SVPWM) controlled the inverter schemes [12-13]. In spite of the limitations of PWM techniques that the carrier phase shift (CPS-PWM) and carrier in-phase disposition (IPD-PWM) modulation techniques can be implemented to Cascaded H-bridge multilevel inverters [14-15]. In order to assess THD, repeated measures were used. Hence, the previous studies have been based their criteria for selection on type of multilevel inverter and on the other hand in most recent studies THD has been measured for different inverter type modification. Just over 5% of THD was acceptable [16-18].
The power quality of the voltage and current signals is improved according to the number of inverter level [19]. Since the output is closer to sinusoidal wave. Consequently, the inverter efficiency and output power have an effectiveness on THD values. Therefore, it is important to modify the inverter topology gaining acceptable output signals.

Moreover, an incremental conductance algorithm has been used to improve the system performance obtaining a maximum power point tracking (MPPT) from the PV panel. The DC supplies will provide from a PV solar array [20]. Reference [21] improved the output line voltage harmonic characteristics by combining a hybrid of these above-mentioned two techniques. In addition, due to the higher dv/dt output from the switching devices in inverters those results from a high dc link voltage, a multi domain dv/dt filters is designed [18]. Modulation index and power factor are maintained in order to increase the balance of the NP voltage by presenting an efficiency-optimized dual modulation wave carrier-based PWM (DMWPWM) strategy of three-level NPC inverter [22]. Some researches implement a fuzzy logic approach with different modulation index that can eliminate the selective harmonic [23]. A low THD is obtained for multi-level inverter when compared to the two-level inverter [24-26].

This paper covers the harmonic distortion of using multilevel inverter for a BLDC motor supplied by a PV array system. The main disadvantages of the MLI is the constraint of designing the control strategy for the PWM switching circuit. It is a challenge to adopt a solar PV with a multilevel inverter utilizing two topologies, diode clamped multilevel inverter, flying capacitor multilevel inverter that requires a huge number of switches. The control technique works based on space vector modulation switching technique. During the changing of the PV output voltage a high distortion might occur caused by the variation of the environment conditions and for that reason a MPPT introduced to avoid this problem.

2. MATHEMATICAL SYSTEM MODEL

The complete proposed system block diagram is shown in Figure 1. It includes PV array, boost dc-to-dc converter, 3-phase three level inverter, incremental conductance maximum power point tracking (INC-MPPT), SVPWM, and BLDC motor [27].

![Figure 1. Block diagram for solar PV fed BLDC motor drive](image)

2.1. PV Panel and INC-MPPT

The INC algorithm can be summarized as in flow chart as shown in Figure 2 and the simulation model of the implementation of INC with a solar PV boost dc to dc converter is shown in Figure 3. Since The INC algorithm employs the slope of the power-voltage curve of a PV array is equal to zero at the MPP [20] and [28]. The PV characteristics and the simulation results for PV model due to different of irradiance on the I-V and P-V characteristic at constant temperature (25 C°) as well as the effect of variation of temperature on the I-V and P-V characteristic at constant irradiance (1000W/m²) are given in appendix A.

2.1.1. BLDC motor

For a BLDC motor, the direct and quadrature axis inductances are not equal, and the voltage equations are given as the following: There are three stator windings in the stator and a rotor consists of a permanent magnet of the BLDC. Due to the high resistivity rotor, the induced currents are neglected. The voltage equations for a 3-phase BLDC motor in matrix form are [27]:

\[
\begin{bmatrix}
V_a \\
V_b \\
V_c
\end{bmatrix} =
\begin{bmatrix}
R_s & 0 & 0 \\
0 & R_s & 0 \\
0 & 0 & R_s
\end{bmatrix}
\begin{bmatrix}
\ell_a \\
\ell_b \\
\ell_c
\end{bmatrix} +
\begin{bmatrix}
L_{aa} & L_{ab} & L_{ac} \\
L_{ba} & L_{bb} & L_{bc} \\
L_{ca} & L_{cb} & L_{cc}
\end{bmatrix}
\begin{bmatrix}
\frac{d}{dt}i_a \\
\frac{d}{dt}i_b \\
\frac{d}{dt}i_c
\end{bmatrix} +
\begin{bmatrix}
e_a \\
e_b \\
e_c
\end{bmatrix}
\]  

where \(v_a, v_b\) and \(v_c\) are the phase voltages; \(i_a, i_b\) and \(i_c\) are the stator currents; \(e_a, e_b\) and \(e_c\) are the BEMFs; \(R_s\) is the stator winding resistance; \(L_{aa}, L_{bb}\) and \(L_{cc}\) are the self-inductances of the stator windings; \(L_{ab}, L_{ba}, L_{ca}, L_{cb}, L_{bc}\) are the mutual inductances between the windings and No damper windings. By assuming...
equal resistances and inductances for the phases, \( L_{aa} = L_{bb} = L_{cc} = L, \ L_{ab} = L_{ba} = L_{bc} = L_{cb} = L_{cb} = \), the following equations obtained:

\[
\begin{align*}
\begin{bmatrix}
V_a \\
V_b \\
V_c
\end{bmatrix} &= \begin{bmatrix}
Rs & 0 & 0 \\
0 & Rs & 0 \\
0 & 0 & Rs
\end{bmatrix} \begin{bmatrix}
i_a \\
i_b \\
i_c
\end{bmatrix} + \begin{bmatrix}
L & M & M \\
M & L & M \\
M & M & L
\end{bmatrix} \begin{bmatrix}
dt 
\frac{d}{dt} i_a \\
\frac{d}{dt} i_b \\
\frac{d}{dt} i_c
\end{bmatrix} + \begin{bmatrix}
e_a \\
e_b \\
e_c
\end{bmatrix}
\end{align*}
\]

(2)
The 3 stator phase currents are controlled to be balanced,

\[ i_a + i_b + i_c = 0 \quad \text{and} \quad i_b + i_c = -i_a \]

\[
\begin{bmatrix}
V_a \\
V_b \\
V_c
\end{bmatrix} =
\begin{bmatrix}
R_s & 0 & 0 \\
0 & R_s & 0 \\
0 & 0 & R_s
\end{bmatrix}
\begin{bmatrix}
i_a \\
i_b \\
i_c
\end{bmatrix} +
\begin{bmatrix}
L - M & 0 & 0 \\
0 & L - M & 0 \\
0 & 0 & L - M
\end{bmatrix}
\frac{d}{dt}
\begin{bmatrix}
i_a \\
i_b \\
i_c
\end{bmatrix} +
\begin{bmatrix}
e_a \\
e_b \\
e_c
\end{bmatrix} \tag{3}
\]

The equations for the BEMFs for BLDC motor are given by:

\[
\begin{bmatrix}
e_a \\
e_b \\
e_c
\end{bmatrix} = \omega_m \lambda_m
\begin{bmatrix}
f_a(\theta_r) \\
f_b(\theta_r) \\
f_c(\theta_r)
\end{bmatrix} \tag{4}
\]

Where \( \omega_m \) the mechanical rotor speed in rad/sec, 
\( \lambda_m \) is the magnetic flux linkage, 
\( \theta_r \) is the rotor position in radian and the functions \( f_a(\theta_r), f_b(\theta_r) \) and \( f_c(\theta_r) \) with a trapezoidal shape having an amplitude of \pm 1.

The electromagnetic torque is given as:

\[ T_e = \frac{e_a i_a + e_b i_b + e_c i_c}{\omega_m} \tag{5} \]

\[ J \frac{d \omega_m}{dt} + B \omega_m = T_e - T_L \tag{6} \]

Where moment of inertia is \( J \), friction coefficient is \( B \), and load torque is \( T_L \)

The simulation schematic diagram is shown in Figure 4.

![Figure 4. BLDC matlab/Simulink model](image)

**2.1.2. Three level inverter with SVPWM**

Two inverter topologies have been considered in this paper; Figure 5 shows the schematic block diagram of the 3-phase three level diode clamped inverter topology [18]. Figure 6 shows the schematic block diagram of the 3-phase three level diode clamped inverter topology [29-31].
SVPWM technique is used extensively for its low switching loss, high flexibility and low computational complexity [17]. PWM technique finds the average variation of voltage space vector. The general structure is shown in the Figure 7. It can be shown that each inverter leg contains two switches, using the combination of these switches eight switching states will be generated that will produce a PWM waveform such that the average variation in the phase will be sinusoidal. In these switching states there are six active states and two zero states, and they can be represented as a hexagonal shape in a two dimensional plane. The hexagon is divided into six sectors the radius is equal to the voltage space vector of the three-phase inverter.

In Figure 7 the 3-phase output voltages are represented in one reference vector that is \( V_{\text{ref}} \) and this vector is rotating in an angular velocity \( \omega = 2\pi f \). The main objective of the space vector modulation is to estimate the reference vector, and this can be done using the switching combination, the approximation is done by switching between any two adjacent active vectors and the zero or null vector. Based on that, the following equations are represented as:

\[
T_1 V_1 + T_2 V_2 + T_0 V_{0,7} = T_s V_{\text{ref}}
\]
\[
T_1 + T_2 + T_0 = T_s
\]

In which \( T_1, T_2 \) and \( T_0 \) are the duty-times for the active voltage vector \( V_1, V_2 \) and the zero-voltage vector \( V_{0,7} \) in the one PWM period ( \( T_s \) ) is the switching time. In the space vector PWM a rotating voltage vector is used as a reference and this vector is sampled once in every sub cycle \( T_s \). Based on the equations above there are two operating conditions for the inverter that is if \( T_1 + T_2 < T_s, T_0 > 0 \) then the inverter is
said to be in the linear modulation mode and this mode contains sufficient modulation margin to pursue the reference vector. When $T_1 + T_2 > T_0, T_0 < 0$ this is known as the over modulation mode.

![Figure 7. Eight switching states of the inverter](image)

2.1.3. Simulation results and discussion

Matlab / Simulink simulation model is shown in Figure 8. The implementation is carried out on the motor that has parameters are given as the following: $R_s = 9.62 \times 10^{-3} \Omega$, direct axis inductance $L_d = 28.7 \times 10^{-6} H$, quadrature axis inductance $L_q = 47.2 \times 10^{-6} H$, number of pole pair $P_b = 6$, moment of inertia $J=20.17 \text{ kg.m}^2$, permanent magnet flux-linkage $\psi_m = 9.71 \times 10^{-3} Wb$ and viscous friction coefficient $B=0 \text{ N.m.s}$. The drive system uses a space vector PWM inverter with a switching frequency of 5kHz and dc-bus voltage of 200V.

The PV panel with its specifications that given as:
Peak power=300W; open circuit voltage=44.6V; MPP voltage= 36.34V; short circuit current= 8.7A; MPP current = 7.8A

The boost dc to dc converter parameters that given as:
Boost inductor= 2.2mH; DC bus capacitor=500 $\mu$F; switching frequency=20kHz.

![Figure 8. Block diagram control for solar PV fed BLDC motor drive](image)

Case 1: 3-phase three level diode-clamped inverter

The simulation results inverter schematic diagram illustrated in Figure 1(a) that fed the BLDC motor and supplied from a PV with MPPT boost dc-to-dc converter. The line voltage waveforms are shown in
Figure 9. The 3-phase current signal and the harmonic spectra of the current signal at modulation index (MI) of 1.4 are shown in Figure 10(a) and (b). It can be achieved that the THD for the current signal is 5.27%.

From Figure 9(b), it can be seen that there is a clear trend of decreasing THD to 5.27% when a multilevel inverter is implemented. This result is significant at the irradiance of 1000W/m² at 25°C.

Case 2: 3-phase three-level flying capacitor inverter

The simulation results inverter schematic diagram illustrated in Figure 1(b) that fed the BLDC motor and supplied from a PV with maximum power point tracking boost dc-to-dc converter. The line voltage waveforms are shown in Figure 11. The 3-phase current signal and the harmonic spectra of the current signal at modulation index of 1.4 are shown in Figure 12(a) and (b). It can be achieved that the THD for the current signal is 13.92%. It is difficult to explain this result, but it might be related to unbalanced voltage.

For the above results, when the three level inverter is operating under steady state conditions with SVPWM within a switching interval for each inverter. Together these results provide and indicate an important insights into switching losses that associated with the flying capacitor inverter has a higher compared to diode clamped inverter. In addition, in order to overcome the MI limitation in SVPWM, the isolated dc voltage has to be modified to improve the voltage profile.

Figure 9. Simulation results of voltage

Figure 10. (a) Simulation results of 3-phase current (b) Harmonic spectra for current signal
3. CONCLUSION

This paper discusses the 3-phase three level inverter topologies that implemented with a solar PV fed a BLDC motor drive. In order to prove their effectiveness respecting the primarily objective to current THD, and they can be used in industrial applications. The results have shown an improved utilization of the dc-bus voltage, still the overshoot is a little bit high in two types of inverter that are proposed. It has been seen that the multilevel clamped diode inverter type can work with a good dynamic comparing to flying capacitor inverter type. The simulation results suggest that a multilevel inverter can be develop THD. It is also showed that a good quality of voltage signal can be obtained for 3-phase three level diode-clamped inverter about 5.2% compared with that of THD 13.92% for flying capacitor inverter. It can be concluded that clamped diode inverter topology is efficient as it assures satisfy harmonic distortion. A Matlab/Simulink was carried out to model the system.

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Appendix A PV characteristics simulation results.
Figure A-1 shows the variation of irradiance on I-V and P-V characteristic at constant temperature. Figure A2 shows Different of temperature on the I-V and P-V characteristic at constant irradiance.

Figure A1. Different of irradiance on the I-V and P-V characteristic at constant temperature (25°C)

Figure A2. Different of temperature on the I-V and P-V characteristic at constant irradiance (1000W/m²)