Apollo: Transferable Architecture Exploration

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Abstract

The looming end of Moore’s Law and ascending use of deep learning drives the design of custom accelerators that are optimized for specific neural architectures. Architecture exploration for such accelerators forms a challenging constrained optimization problem over a complex, high-dimensional, and structured input space with a costly to evaluate objective function. Existing approaches for accelerator design are sample-inefficient and do not transfer knowledge between related optimizations tasks with different design constraints, such as area and/or latency budget, or neural architecture configurations. In this work, we propose a transferable architecture exploration framework, dubbed APOLLO, that leverages recent advances in black-box function optimization for sample-efficient accelerator design. We use this framework to optimize accelerator configurations of a diverse set of neural architectures with alternative design constraints. We show that our framework finds high reward design configurations (up to 24.6% speedup) more sample-efficiently than a baseline black-box optimization approach. We further show that by transferring knowledge between target architectures with different design constraints, APOLLO is able to find optimal configurations faster and often with better objective value (up to 25% improvements). This encouraging outcome portrays a promising path forward to facilitate generating higher quality accelerators.

1 Introduction

The ubiquity of customized accelerators demands efficient architecture exploration approaches, especially for the design of neural network accelerators. However, optimizing the parameters of accelerators is daunting optimization task that generally requires expert knowledge [11, 28]. This complexity in the optimization is because the search space is exponentially large while the objective function is a black-box and costly to evaluate. Constraints imposed on parameters further convolute the identification of valid accelerator configurations. Constrains can arise from hardware limitations or if the evaluation of a configuration is impossible or too expensive [29].

To address the aforementioned challenges, we introduce a general accelerator architecture exploration framework, dubbed APOLLO, that leverages the recent advances in black-box optimization to facilitate finding optimal design configurations under different design constraints. We demonstrate how leveraging tailored optimization strategies for complex and high-dimensional space of architecture exploration yields large improvements (up to 24.6%) with a reasonably small number of evaluations (≈ 0.0004% of the search space). Finally, we present the very first study on the impact of transfer learning between architecture exploration tasks with different design constraints in further reducing.
the number of hardware evaluations. The following outlines the contributions of APOLLO, making
the first transferable architecture exploration infrastructure:

- **End-to-end architecture exploration framework.** We introduce and develop APOLLO, an end-
  to-end and highly configurable framework for architecture exploration. The proposed framework
  tunes accelerator configurations for a target set of workloads with a relatively small number of
  hardware evaluations. As hardware simulations are generally time-consuming and expensive to
  obtain, reducing the number of these simulations not only shortens the design cycle for accelerators,
  but also provides an effective way to adapt the accelerator itself to various target workloads.

- **Supporting various optimization strategies.** APOLLO introduces and employs a variety of opti-
  mization strategies to facilitate the analysis of optimization performance in the context of architecture
  exploration. Our evaluations results show that evolutionary and population-based black-box optimization
  strategies yield the best accelerator configurations (up to 24.6% speedup) compared to a baseline
  black-box optimization with only \( \approx 2K \) number of hardware evaluations (\( \approx 0.0004\% \) of search space).

- **Transfer learning for architecture exploration.** Finally, we study and explore transfer learning
  between architecture exploration tasks with different design constraints showing its benefit in
  improving the optimization results and sample-efficiency. Our results show that transfer learning
  not only improves the optimization outcome (up to 25\%) compared to independent exploration,
  but also reduces the number of hardware evaluations.

2 Methodology

**Problem definition.** The objective in APOLLO (architecture exploration) is to discover a set of feasible
accelerator parameters \( (h) \) for a set of workloads \( (w) \) such that a desired objective function \( (f) \), e.g.
weighted average of runtime, is minimized under an optional set of user-defined constraints, such
as area \( (\alpha) \) and/or runtime budget \( (\tau) \).

\[
\min_{h,w} f(h, w) \\
\text{s.t. } \text{Area}(h) \leq \alpha \\
\text{Latency}(h, w) \leq \tau
\]

The manifold of architecture search generally contains infeasible points [28], for example due to
impractical hardware implementation for a given set of parameters or impossible mapping of workloads
to an accelerator. As such, one of the main challenges for architecture exploration is to effectively
sidestep these infeasible points. We present and analyze the performance of optimization strategies to
reduce the number of infeasible trials in Section 3.

**Neural models.** We evaluate APOLLO on two variations of MobileNet [33, 15] models and five
in-house neural networks with distinct accelerator resource requirements. The neural model
configurations, including their target domain, number of layers, and total filter sizes are detailed in
Table 1. In the multi-model study, the workload contains MobileNetV2 [33], MobileNetEdge [15],
M3, M4, M5, M6, and M7.

| Name             | Domain               | # of layers | Params (MB) | # of MACs |
|------------------|----------------------|-------------|-------------|-----------|
| MobileNetV2 [33] | Image Classification | 76          | 3.33        | 301 M     |
| MobileNetEdge [16]| Image Classification | 93          | 3.88        | 991 M     |
| M3               | Object Detection     | 93          | 2.19        | 464 M     |
| M4               | Object Detection     | 111         | 0.42        | 107 M     |
| M5               | Object Detection     | 60          | 6.29        | 1721 M    |
| M6               | Semantic Segmentation| 62          | 0.37        | 591 M     |
| M7               | OCR                  | 56          | 0.30        | 5.19 M    |

**Accelerator search space.** In this work, we use an in-house and highly parameterized edge accelerator.
The accelerator contains a 2D array of processing elements (PE) with multiple compute lanes and
dedicated register files, each operating in single-instruction multiple-data (SIMD) style with multiply-
accumulate (MAC) compute units. There are distributed local and global buffers that are shared across
the compute lanes and PEs, respectively. We designed a cycle-accurate simulator that faithfully models the main microarchitectural details and enables us to perform architecture exploration. Table 2 outlines the microarchitectural parameters (e.g. compute, memory, or bandwidth) and their number of discrete values in the search space. The total number of design points explored in APOLLO is nearly $5 \times 10^8$.

Table 2: The microarchitecture parameters, their type, and number of discrete values per parameter. The total number of design points per each study is 452,760,000.

| Accelerator Parameter | # discrete values | Accelerator Parameter | # discrete values |
|-----------------------|------------------|-----------------------|------------------|
| # of PEs-X            | 10               | # of PEs-Y            | 10               |
| Local Memory          | 7                | # of SIMD units       | 7                |
| Global Memory         | 11               | # of Compute lanes    | 10               |
| Instruction Memory    | 4                | Parameter Memory      | 5                |
| Activation Memory     | 7                | I/O Bandwidth         | 6                |

2.1 Optimization Strategies

In APOLLO, we study and analyze the performance of following optimization methods.

**Evolutionary.** Performs evolutionary search using a population of $K$ individuals, where the genome of each individual corresponds to a sequence of discretized accelerator configurations. New individuals are generated by selecting for each individual two parents from the population using tournament selecting, recombining their genomes with some crossover rate $\gamma$, and mutating the recombined genome with some probability $\mu$. Following Real et al. [31], individuals are discarded from the population after a fixed number of optimization rounds (‘death by old age’) to promote exploration. In our experiments, we use the default parameters $K=100$, $\gamma=0.1$, and $\mu=0.01$.

**Model-Based Optimization (MBO).** Performs model-based optimization with automatic model selection following [2]. At each optimization round, a set of candidate regression models are fit on the data acquired so far and their hyper-parameter optimized by randomized search and five fold cross-validation. Models with a cross-validation score above a certain threshold are ensembled to define an acquisition function. The acquisition is optimized by evolutionary search and the proposed accelerator configurations with the highest acquisition function values are used for the next objective function evaluation.

**Population-Based black-box optimization (P3BO).** Uses an ensemble of optimization methods, including Evolutionary and MBO, which has been recently shown to increase sample-efficiency and robustness [3]. Acquired data are exchanged between optimization methods in the ensemble, and optimizers are weighted by their past performance to generate new accelerator configurations. Adaptive-P3BO is an extension of P3BO which further optimizes the hyper-parameters of optimizers using evolutionary search, which we use in our experiments.

**Random.** Samples accelerator configurations uniformly at random from the defined search space.

**Vizier.** An alternative approach to MBO based on Bayesian optimization with a Gaussian process regressor and the expected improvement acquisition function, which is optimized by gradient-free hill-climbing [14]. Categorical variables are one-hot encoded.

We use the Google Vizier framework [14] with the optimization strategies described above for performing our experiments. We use the default hyper-parameter of all strategies [14, 3]. Each optimization strategy is allowed to propose 4096 trials per experiment. We repeat each experiment five times with different random seeds and set the reward of infeasible trials to zero. To parallelize hardware simulations, we use 256 CPU cores each handling one hardware simulation at a time. We further run each optimization experiment asynchronously with 16 workers that can evaluate up to 16 trials in parallel.

3 Evaluation

**Single model architecture search.** For the first experiment, we define the optimization problem as maximizing throughput per area (e.g. $\frac{1}{\text{latency}} \times \frac{1}{\text{area}}$) for each neural model without defining any design constraints. Figure 1 depicts the cumulative reward across various number of trials. Compared to Vizier, Evolutionary and P3BO improve the throughput per area by 4.3% (up to 12.2% in MobileNetV2), on average. In addition, both Evolutionary and P3BO yield lower variance across multiple runs suggesting a more robust optimization method for architecture search.
Multi-model architecture search. For multi-model architecture search, we define the optimization as maximizing \( \text{geomean(speedup)} \) across all the evaluated models (See Section 2) while imposing area budget constraints of 6.8 mm\(^2\), 5.8 mm\(^2\), and 4.8 mm\(^2\). Note that, as the area budget becomes stricter, the number of infeasible trials increases. The baseline runtime numbers are obtained from a productionized edge accelerator. Figure 2 demonstrates the cumulative reward (e.g., \( \text{geomean(speedup)} \)) across various number of sampled trials. Across the studied optimization strategies, P3BO delivers the highest improvements across all the design constraints. Compared to Vizier, P3BO improves the speedup by 6.2\%, 16.6\%, and 24.6\% for area budget 6.8 mm\(^2\), 5.8 mm\(^2\), and 4.8 mm\(^2\), respectively. These results demonstrate that as the design space becomes more constrained (e.g., more infeasible points), the improvement by P3BO increases, showing its performance in navigating the search space better.

Analysis of infeasible trials. To better understand the effectiveness of each optimization strategy in selecting feasible trials and unique trials, we define two metrics feasibility ratio and uniqueness ratio, respectively. The feasibility (uniqueness) ratio defines the fraction of feasible (unique) trials over the total number of sampled trials. Higher ratios generally indicate improved exploration of feasible regions. Table 3 summarizes the feasibility and uniqueness ratio of each optimization strategy for area budget 6.8 mm\(^2\), averaged over multiple optimization runs. MBO yields the highest avg. feasibility ratio of \( \approx 0.803 \) while Random shows the lowest ratio of \( \approx 0.009 \). While MBO features a high feasibility ratio, it underperforms compared to other optimization strategies in finding accelerator configurations with high performance. The key reason attributed to this behavior for MBO is its low performance (0.236) in identifying unique accelerator parameters compared to other optimization strategies.

Table 3: The average feasibility and uniqueness ratio across five runs for architecture search with an area budget of 6.8 mm\(^2\) (see Figure 2a).

|                      | Evolutionary | MBO  | P3BO | Random | Vizier |
|----------------------|--------------|------|------|--------|--------|
| Avg. Feasibility Ratio (↑ better) | 0.362        | 0.803| 0.347| 0.009  | 0.012  |
| Avg. Uniqueness Ratio (↑ better)  | 0.891        | 0.236| 0.848| 1.0    | 0.979  |

Diversity of architecture configurations. A desired property of optimizers is to not only find a single but a diverse set of architecture configurations with a high reward that can be tested downstream. We quantified the ability of optimizers to find diverse configurations qualitatively by visualizing the 50 best unique trials found by each method using tSNE. Figure 3a shows that Evolutionary and P3BO find both higher-reward and more diverse configurations compared to alternative methods with the exception of Random. This finding is supported quantitatively by Figure 3b, which shows the mean pairwise
Figure 2: Performance of optimization strategies in maximizing $\text{geomean(speedup)}$ ($\uparrow$ is better) under alternative area budget constraints. The shaded area depicts the 95% bootstrap confidence interval over five runs. The baseline latency numbers are from a productionized edge accelerator. As the area constraint becomes tighter (more infeasible points), the improvement by P3BO increases.

(a) Area Budget = 6.8
(b) Area Budget = 5.8
(c) Area Budget = 4.8

Figure 3: Diversity quantification of architecture configurations found by different methods for an area budget of 4.8 mm$^2$.

Euclidean distance of configurations with a reward above the 75th percentile of the maximum reward. The mean pairwise distance of Random is zero since it did not find any configurations with a reward above the 75th percentile. To further visualize the search space in architecture exploration, Figure 4 shows the tSNE visualization of all trials proposed by the Evolutionary method for an area budget of 4.8 mm$^2$. This figure shows the large number of infeasible trials in the space and the proximity of low- and high-performing trials, which renders identifying high-performing trials challenging.

Transfer learning between optimizations with different constraints. We analyze the effect of transfer learning between architecture search tasks with different area budgets. To create the source tasks, we select 100 unique trials from optimization studies with area budget constraint of 6.8 mm$^2$ (See Fig. 2a) under two criteria. First, the area consumption of the selected trials must satisfy the area budget (4.8 mm$^2$) of the target task. Second, the objective function value (reward) of the selected trials must be below a predefined threshold. In our experiments, we create two source tasks with an objective value of 0.8 and 0.4, respectively, which we chose to better understand the impact of low- and high-value rewards. We use the selected trials to seed the optimization of the target task, which has an area budget of 4.8 mm$^2$). Figure 5 shows the results. All the optimization strategies find high reward trials in fewer steps with transfer learning than without. The improvement is most pronounced for Vizier, which finds trials with a reward of $\approx 1.0$ with transfer learning compared to only $\approx 0.8$ without transfer learning. This suggest that Vizier uses the selected trials from the source task more efficiently than Evolutionary and P3BO for optimizing the target task.

In our implementation, Evolutionary and P3BO simply use the 100 unique and feasible trials from the source task to initialize the population of evolutionary search. Instead, Vizier uses a more advanced transfer learning approach based on a stack of Gaussian process regressors (see Section 3.3 of Golovin et al. [14]), which may account for the performance improvement. We leave extending Evolutionary and P3BO by more advanced transfer learning approaches as future work.
Comparison to exhaustive exploration. To understand the optimal design point, we perform a semi-exhaustive search within the search space. Since the search space has almost $5 \times 10^8$ design points, it is merely not practical to perform a fully-exhaustive search. As such, we manually prune the search space using domain knowledge where the design points are within a typical edge accelerator configuration (e.g. total memory size within 4–16 MB, total number of PEs within 2–16, etc.). Additionally, we perform a cheaper area estimation to reject design points before performing expensive cycle-level simulations. Using this pruning approach, we reduced the size of search space to around 3K samples. We observe that P3BO can reach the best configurations found by the semi-exhaustive search by performing far fewer evaluations ($1.36 \times$ less). Another interesting observation is that for the multi-model experiment targeting 6.8 mm$^2$, P3BO actually finds a design slightly better than semi-exhaustive with 3K-sample search space. We observe that the design uses a very small memory size (3MB) in favor of more compute units. This leverages the compute-intensive nature of vision workloads, which was not included in the original semi-exhaustive search space. This demonstrates the need of manual search space engineering for semi-exhaustive approaches, whereas learning-based optimization methods leverage large search spaces reducing the manual effort.

4 Related Work

While inspired by related work, APOLLO is fundamentally different from classic methodologies in design space exploration: (1) we develop a platform to compare the effectiveness of a wide range of optimization algorithms; and (2) we are the first work, to the best of our knowledge, that leverages transfer learning between architecture exploration tasks with different design constraints showing how transfer learning slashes the time for discovering new accelerator configurations. Related work to APOLLO embodies three broad research categories of black-box optimization, architecture exploration, and transfer learning. Below, we overview the most relevant work in these categories.
**Black-box optimization.** Black-box optimization has been broadly applied across different domains and appeared under various optimization categories, including Bayesian [37, 3, 24, 34, 42, 36, 6, 8], evolutionary [1, 39, 20], derivative-free [23, 32, 12], and bandit [7, 25, 38, 13]. APOLLO benefits from advances in black-box optimization and establishes a basis for leveraging this broad range of optimization algorithms in the context of accelerator design. In this work, we extensively studied the effectiveness of some of these black-box optimization algorithms, namely random search [14], Bayesian optimization [14], evolutionary algorithms [3], and ensemble methods [3] in discovering optimal accelerator configurations under different design objectives and constraints.

**Design space exploration.** Design space exploration in computer systems has been always an active research and has become even more crucial due to the surge of specialized hardware [30, 18, 40, 28, 10, 21, 5, 4]. Hierarchical-PABO [30] and FlexiBO [18] use multi-objective Bayesian optimization for neural network accelerator design. In order to reduce the use of computational resources, Sun et al. [40] apply genetic algorithm to design CNN models without modifying the underlying architecture. HyperMapper [28] uses a random forest in the automatic tuning of hardware accelerator parameters in a multi-objective setting. HyperMapper optionally uses continuous distributions to model the search space variables as a means to inject prior knowledge into the search space.

**Transfer learning.** Transfer learning exploits the acquired knowledge in some tasks to facilitate solving similar unexplored problems more efficiently, e.g. consuming a fewer number of data samples and/or outperforming previous solutions. Transfer learning has been explored extensively and applied to various domains [27, 44, 43, 17, 19, 9, 35, 26, 22, 41]. Due to the expensive-to-evaluate nature of hardware evaluations, transfer learning seems to be a practical mechanism for architecture exploration. However, using transfer learning for architecture exploration and accelerator design is rather less explored territory. APOLLO is one of the first methods to bridge this gap between transfer learning and architecture exploration.

5 Conclusion

In this paper, we propose APOLLO, a framework for sample-efficient architecture exploration for large scale design spaces. The benefits of APOLLO are most noticeable when architecture configurations are costly to evaluate, which is a common trait in various architecture optimization problems. Our framework also facilitates the design of new accelerators with different design constraints by leveraging transfer learning. Our results indicate that transfer learning is effective in improving the target architecture exploration, especially when the optimization constraints have tighter bounds. Finally, we show that the evolutionary algorithms used in this work yield more diverse accelerator designs compared to other studied optimization algorithms, which can potentially discover overlooked architectures. Architecture exploration is just one use case in the accelerator design process that is bolstered by APOLLO. The evolution of accelerator architectures mandates broadening the scope of optimizations to the entire computing stack, including scheduling and mapping, that potentially yields higher benefits at the cost of handling more complex optimization problems. We argue that such co-evolution between the cascaded layers of the computing stack is inevitable in designing efficient accelerators honed for a diverse category of applications. This is an exciting path forward for future research directions.

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References

[1] Harith Al-Sahaf, Ying Bi, Qi Chen, Andrew Lensen, Yi Mei, Yanan Sun, Binh Tran, Bing Xue, and Mengjie Zhang. A survey on evolutionary machine learning. *Journal of the Royal Society of New Zealand*, 49(2):205–228, 2019.

[2] Christof Angermueller, David Dohan, David Belanger, Ramya Deshpande, Kevin Murphy, and Lucy Colwell. Model-based reinforcement learning for biological sequence design. In *International Conference on Learning Representations*, 2019.

[3] Christof Angermueller, David Belanger, Andreea Gane, Zelda Mariet, David Dohan, Kevin Murphy, Lucy Colwell, and D Sculley. Population-based black-box optimization for biological sequence design. *arXiv preprint arXiv:2006.03227*, 2020.
[4] Jason Ansel, Shoaib Kamil, Kalyan Veeramachaneni, Jonathan Ragan-Kelley, Jeffrey Bosboom, Una-May O’Reilly, and Saman Amarasinghe. OpenTuner: An extensible framework for program autotuning. In *Proceedings of the 23rd international conference on Parallel architectures and compilation*, pp. 303–316, 2014.

[5] Prasanna Balaprakash, Ananta Tiwari, Stefan M Wild, Laura Carrington, and Paul D Hovland. AutoMOMML: Automatic multi-objective modeling with machine learning. In *International Conference on High Performance Computing*, pp. 219–239. Springer, 2016.

[6] James S Bergstra, Rémi Bardenet, Yoshua Bengio, and Balázs Kégl. Algorithms for hyper-parameter optimization. In *Advances in neural information processing systems*, pp. 2546–2554, 2011.

[7] Djallel Boureifouf and Irina Rish. A survey on practical applications of multi-armed and contextual bandits. *arXiv preprint arXiv:1904.10040*, 2019.

[8] Eric Brochu, Vlad M Cora, and Nando De Freitas. A tutorial on bayesian optimization of expensive cost functions, with application to active user modeling and hierarchical reinforcement learning. *arXiv preprint arXiv:1012.2599*, 2010.

[9] T. Chugh, M. Singh, S. Nagpal, R. Singh, and M. Vatsa. Transfer learning based evolutionary algorithm for composite face sketch recognition. In *2017 IEEE Conference on Computer Vision and Pattern Recognition Workshops (CVPRW)*, pp. 619–627, 2017.

[10] Jason Cong, Peng Wei, Cody Hao Yu, and Peng Zhang. Automated accelerator generation and optimization with composable, parallel and pipeline architecture. In *2018 55th ACM/ESDA/IEEE Design Automation Conference (DAC)*, pp. 1–6. IEEE, 2018.

[11] Andrew R Conn, Katya Scheinberg, and Luis N Vicente. *Introduction to derivative-free optimization*. SIAM, 2009.

[12] Andrew R Conn, Katya Scheinberg, and Luis N Vicente. *Introduction to derivative-free optimization*. SIAM, 2009.

[13] Josep Ginebra and Murray K Clayton. Response surface bandits. *Journal of the Royal Statistical Society: Series B (Methodological)*, 57(4):771–784, 1995.

[14] Daniel Golovin, Benjamin Solnik, Subhodeep Moitra, Greg Kochanski, John Karro, and D Sculley. Google vizier: A service for black-box optimization. In *Proceedings of the 23rd ACM SIGKDD international conference on knowledge discovery and data mining*, pp. 1487–1495, 2017.

[15] Suyog Gupta and Berkin Akin. Accelerator-aware neural network design using automl. *arXiv preprint arXiv:2003.02838*, 2020.

[16] Andrew Howard and Suyog Gupta. Introducing the Next Generation of On-Device Vision Models: MobileNetV3 and MobileNetEdgeTPU. *https://ai.googleblog.com/2019/11/introducing-next-generation-on-device.html*, 2020.

[17] Kotthoff Lars Vanschoren Joaquin Hutter, Frank (ed.). *Automated Machine Learning: Methods, Systems, Challenges*. The Springer Series on Challenges in Machine Learning. Springer International Publishing, 2019.

[18] Md Shahriar Iqbal, Jianhai Su, Lars Kotthoff, and Pooyan Jamshidi. Flexibo: Cost-aware multi-objective optimization of deep neural networks. *arXiv preprint arXiv:2001.06588*, 2020.

[19] Min Jiang, Zhongqiang Huang, Liming Qiu, Wenzhen Huang, and Gary G Yen. Transfer learning-based dynamic multiobjective optimization algorithms. *IEEE Transactions on Evolutionary Computation*, 22(4):501–514, 2017.

[20] Donald R Jones, Matthias Schonlau, and William J Welch. Efficient global optimization of expensive black-box functions. *Journal of Global optimization*, 13(4):455–492, 1998.
[21] David Koeplinger, Matthew Feldman, Raghu Prabhakar, Yaqi Zhang, Stefan Hadjis, Ruben Fiszel, Tian Zhao, Luigi Nardi, Ardavan Pedram, Christos Kozyrakis, et al. Spatial: A language and compiler for application accelerators. In Proceedings of the 39th ACM SIGPLAN Conference on Programming Language Design and Implementation, pp. 296–311, 2018.

[22] Barış Koçer and Ahmet Arslan. Genetic transfer learning. Expert Systems with Applications, 37(10):6997–7002, October 2010.

[23] Jeffrey Larson, Matt Menickelly, and Stefan M Wild. Derivative-free optimization methods. arXiv preprint arXiv:1904.11585, 2019.

[24] Benjamin Letham, Brian Karrer, Guilherme Ottoni, Eytan Bakshy, et al. Constrained bayesian optimization with noisy experiments. Bayesian Analysis, 14(2):495–519, 2019.

[25] Lisha Li, Kevin Jamieson, Giulia DeSalvo, Afshin Rostamizadeh, and Ameet Talwalkar. Hyperband: A novel bandit-based approach to hyperparameter optimization. The Journal of Machine Learning Research, 18(1):6765–6816, 2017.

[26] Jie Lu, Vahid Behbood, Peng Hao, Hua Zuo, Shan Xue, and Guangquan Zhang. Transfer learning using computational intelligence: A survey. Knowledge-Based Systems, 80:14–23, May 2015.

[27] Alan Tan Wei Min, Yew-Soon Ong, Abhishek Gupta, and Chi-Keong Goh. Multiproblem Surrogates: Transfer Evolutionary Multiobjective Optimization of Computationally Expensive Problems. IEEE Transactions on Evolutionary Computation, 23(1):15–28, February 2019.

[28] Luigi Nardi, David Koeplinger, and Kunle Olukotun. Practical design space exploration. In 2019 IEEE 27th International Symposium on Modeling, Analysis, and Simulation of Computer and Telecommunication Systems (MASCOTS), pp. 347–358. IEEE, 2019.

[29] Angshuman Parashar, Priyanka Raina, Yakun Sophia Shao, Yu-Hsin Chen, Victor A Ying, Anurag Mukkara, Ranharajan Venkatesan, Brucek Khailany, Stephen W Keckler, and Joel Emer. Timeloop: A systematic approach to dnn accelerator evaluation. In ISPASS. IEEE, 2019.

[30] Maryam Parsa, John P Mitchell, Catherine D Schuman, Robert M Patton, Thomas E Potok, and Kaushik Roy. Bayesian multi-objective hyperparameter optimization for accurate, fast, and efficient neural network accelerator design. Frontiers in Neuroscience, 14:667, 2020.

[31] Esteban Real, Alok Aggarwal, Yanping Huang, and Quoc V Le. Regularized evolution for image classifier architecture search. In Proceedings of the aaai conference on artificial intelligence, volume 33, pp. 4780–4789, 2019.

[32] Luis Miguel Rios and Nikolaos V Sahinidis. Derivative-free optimization: a review of algorithms and comparison of software implementations. Journal of Global Optimization, 56(3):1247–1293, 2013.

[33] Mark Sandler, Andrew Howard, Menglong Zhu, Andrey Zhmoginov, and Liang-Chieh Chen. Mobilenetv2: Inverted residuals and linear bottlenecks. In Proceedings of the IEEE conference on computer vision and pattern recognition, pp. 4510–4520, 2018.

[34] Bobak Shahriari, Kevin Swersky, Ziyu Wang, Ryan P Adams, and Nando De Freitas. Taking the human out of the loop: A review of bayesian optimization. Proceedings of the IEEE, 104(1):148–175, 2015.

[35] Alistair Shilton, Sunil Gupta, Santu Rana, and Svetla Venkatesh. Regret bounds for transfer learning in bayesian optimisation. In Machine Learning Research: Proceedings of the 20th Artificial Intelligence and Statistics International Conference, pp. 1–9. Journal of Machine Learning Research (JMLR), 2017.

[36] Jasper Snoek, Hugo Larochelle, and Ryan P Adams. Practical bayesian optimization of machine learning algorithms. In Advances in neural information processing systems, pp. 2981–2989, 2012.

[37] Artur Souza, Luigi Nardi, Leonardo B Oliveira, Kunle Olukotun, Marius Lindauer, and Frank Hutter. Prior-guided bayesian optimization. arXiv preprint arXiv:2006.14608, 2020.
[38] Niranjan Srinivas, Andreas Krause, Sham M Kakade, and Matthias Seeger. Gaussian process optimization in the bandit setting: No regret and experimental design. *arXiv preprint arXiv:0912.3995*, 2009.

[39] Chaoli Sun, Yaochu Jin, and Ying Tan. Semi-supervised learning assisted particle swarm optimization of computationally expensive problems. In *Proceedings of the Genetic and Evolutionary Computation Conference*, pp. 45–52, 2018.

[40] Yanan Sun, Bing Xue, Mengjie Zhang, Gary G Yen, and Jiancheng Lv. Automatically designing cnn architectures using the genetic algorithm for image classification. *IEEE Transactions on Cybernetics*, 2020.

[41] Kevin Swersky, Jasper Snoek, and Ryan P Adams. Multi-task bayesian optimization. In *Advances in neural information processing systems*, pp. 2004–2012, 2013.

[42] Ke Tang, Fei Peng, Guoliang Chen, and Xin Yao. Population-based algorithm portfolios with automated constituent algorithms selection. *Information Sciences*, 279:94–104, 2014.

[43] Tinu Theckel Joy, Santu Rana, Sunil Gupta, and Svetha Venkatesh. A flexible transfer learning framework for Bayesian optimization with convergence guarantee. *Expert Systems with Applications*, 115:656–672, January 2019.

[44] Michael Volpp, Lukas P. Fröhlich, Kirsten Fischer, Andreas Doerr, Stefan Falkner, Frank Hutter, and Christian Daniel. Meta-Learning Acquisition Functions for Transfer Learning in Bayesian Optimization. *arXiv:1904.02642 [cs, stat]*, February 2020.