Application of Markowitz Portfolio Theory to Producing the World Major Field Crops

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Abstract

Development of growing cereals and oilseeds is a pressing issue for providing global food security and renewable energy. The study deals with applying methods of portfolio theory to mitigate natural and marketing uncertainties emerged from unstable yields and volatile prices for wheat, maize, barley, sunflower, soybeans, and rapeseed. The research outcome based on the utilization of Markowitz mean-variance indicators made possible to evaluate portfolio performances of the world top cereals and oilseeds producers. The study findings at a country level combined econometric forecasting of the crop revenues and modeling optimal portfolios of cereals and oilseeds subject to acceptable trade-offs between risks and expected revenues. The fulfilled calculations with Ukrainian focus clarified farmland allocations under cereal and oilseed crops to underpin biodiversity and keep firm positions in the world markets.

Keywords

Cereals and oilseeds; risk; production portfolio; revenue forecast; Markowitz models.

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Introduction

The world major field crops are cereals and oilseeds. They are utilized for food, feed, and bio-fuel production. As of 2019, the prime cereal crops like wheat, rice, maize, and barley occupied 214.8, 167.1, 193.7, and 48 million hectares of farmland around the world and were cultivated in 123, 117, 168, and 104 countries respectively. Similarly, the prime oilseed crops such as sunflower, soybeans, and rapeseed covered 26.7, 124.9, and 37.6 million hectares of the world arable land in 73, 99, and 65 countries (FAOStat, 2020).

At the same time, agriculture is a risky business. It implies that farmers have to meet the challenges of output uncertainty caused by the natural factors and price volatility affected by fluctuations of the market supply and demand. The most promising tool to facilitate this issue is a portfolio approach. In case of the agricultural sector, portfolio production can measure a risk, predict revenue, and allocate a restricted resource of farmland on different assets like cash crops. Developing such optimal win-win strategies will comply with the environmental, social, and economic goals of maintaining agricultural biodiversity, providing the global food security in view of the accelerated population growth, and gaining competitive advantages in the domestic and international agricultural markets. Given the pressing aspects of portfolio production of the world major field crops, it is worth a separate thorough scientific study.

Creating risk-efficient operating plans and strategies is a key point in contemporary agriculture. Farmers around the globe are exposed to production, marketing, financial, legal, and personnel risks. Science proposes a wide variety of means and tools to handle such uncertainties. But the most fruitful risk-management decisions are those adjusted to specific agricultural products (Broll et al., 2013).

The European cropping pattern includes the above listed world major cereals and oilseeds except for rice. Given the Ukrainian research focus, this investigation considered wheat, maize, barley, sunflower, soybeans, and rapeseed. Advanced economics of their production, processing, marketing, and utilization was revealed in numerous comprehensive studies, in particular by Carver (2009), Danforth (2011), Elfson (2011),...
Martinez-Force et al. (2015), Johnson et al. (2015), and Gunstone (2004).

Villanueva et al. (2017) clarified that the witnessed biodiversity within the groups of cereals and oilseeds have a positive impact on crops resilience and adaptability to the ongoing climate change. Besides, Brussaard et al. (2010), Frison et al. (2011) indicated importance of biodiversity in providing food security via preventing declines in yields of the core staple crops. In case of Ukraine, biodiversity contributed to robust food security by cereals and oilseeds, unlike other industries of the national agriculture (Vasylieva, 2018; Vasylieva, 2019).

Mathematical models developed by Brummer et al. (2016), Haile et al. (2016), Santeramo and Lamonaca (2019) offered accurate and convincing evidence that risks in supplies dependent on yield fluctuations strongly affect price volatility in cereals and oilseeds markets. In other words, it is crucial to allocate farmland under a mix of crops to match both natural and market conditions (Skrypnyk et al., 2018; Ramankutty et al., 2018).

In this regard, the most appropriate mathematical apparatus is the portfolio concept intended to assist in selecting weights of assets to mitigate possible losses (Kolm et al., 2014). Such approach demonstrates reliable results in modelling diversified crop production. In particular, based on the assumption that “typically, risk in the farm income arises from risk in revenue”, Mumey et al. (1992, p. 71) developed models of reducing revenue risk experienced by the wheat, barley, and canola producers at the local level. Barkley et al. (2010) examined a portfolio of wheat varieties directed at increasing yields, shrinking risk and enhancing profitability. Radulescu et al. (2014) elaborated optimal portfolios under minimum environmental and financial risks or maximum expected returns from growing wheat, corn, barley, sunflower, and rapeseed. Recent findings on this topic included models on mean-variance planning for crop farms (Toth et al., 2016).

However, the world production portfolios of the most demanded cereals and oilseeds need an updated comparison which entails options of the optimal crop portfolios applicable at a country level. In light of the agricultural resources and potentials, the latter was conducted for Ukraine. With this research objective, the study was divided into three tasks:

- to implement Markowitz mean-variance indicators to track progress in performing production portfolios of the world major cereals and oilseeds;
- to forecast fluctuations of revenues from wheat, maize, barley, sunflower, soybeans, and rapeseed caused by unstable yields and price volatility in Ukraine; and
- to utilize Markowitz models for cereals and oilseeds to calculate their production portfolios subject to an acceptable trade-off between risk and expected revenue.

**Materials and methods**

To cope with the task 1, this research employed the mean-variance fundamentals of Markowitz portfolio theory (Markowitz, 2010). In more detail, 
\[ N \]
\[ W_i \]
\[ T \]
\[ X_{it} \]

It made possible to compare portfolio performance among the world top crop producers via expected portfolio revenue (EPR) and portfolio risk (PR) built on the logarithmic indices of crop revenue relative to values in the preceding year:

\[ Z_i^t = \ln(X_i^t / X_{i,t-1}^t), \quad t = 2, ..., T, \]

\[ Z^* = \sum_{t=2}^{T} Z_i^t / (T - 1), \quad i = 1, ..., N. \]

In this fashion, the named portfolio indicators were calculated as follows:

\[ \text{EPR} = \sum_{i=1}^{N} W_i \cdot Z^*, \quad (1) \]

\[ \text{PR} = \frac{\sum_{i=1}^{N} \sum_{j=1}^{N} (W_i \cdot W_j) \cdot \sum_{t=2}^{T} ((Z_i^t - Z^*) \cdot (Z_j^t - Z^*)) / (T - 1)). \quad (2) \]

In addition, an indicator of the present portfolio revenue (PPR) illuminated a current output in absolute terms like

\[ \text{PPR} = \sum_{i=1}^{N} W_i \cdot X_{i,t}^t. \quad (3) \]

The panel data intended for the task 1 involved time-series of revenues from the world major portfolio crops by top countries. A methodical background to the task 2 was econometrics (Greene, 2007; Studenmund, 2016). It was focused on capturing trend and cycle
components of dynamics in crop revenue. For such reason, the offered regression incorporated linear and sinusoidal components such as

$$X(t) = A_0 + A_1 \cdot t + A_2 \cdot \sin(A_3 + A_4 \cdot t).$$  (4)

Here $X(t)$ denoted a calculated crop revenue (in $ per hectare) associated with a time variable $t$. The numerical regression coefficients $A_0 - A_4$ were found through the least squares method applied to the time-series data concerning the analyzed major field crops, i.e.

$$\sum_{i=1}^{T} (X_i - (A_0 + A_1 \cdot t + A_2 \cdot \sin(A_3 + A_4 \cdot t)))^2 \rightarrow \min.$$ (5)

As before, $T$ denoted a time frame, and $X_i$ was a real crop revenue referred to the observation $t$. The regression coefficients allowed comparing dynamics in different crops. Namely, the coefficient $A_1$ described an annual change in a revenue trend. Meanwhile, the coefficient $A_2$ revealed the revenue volatility via a cycle amplitude.

R-squared and F-test verified the regression applicability to forecasting crop revenue over the future periods. In case of inadequate accuracy of calculations, the utilized least squares method should be replaced by its advanced modification.

To arrange a trade-off between the expected portfolio revenue and portfolio risk, the research task 3 dealt with both maximum and minimum Markowitz models (Prigent, 2007). In compliance with the previous identifications, $W_i$, $i = 1, ..., N$ were the model variables associated with the sought shares of crops in production portfolios. The given lower bounds to the share of each crop enabled to promote biodiversity assuming that

$$S_i > 0, i = 1, ..., N, \text{ and } \sum_{i=1}^{N} S_i < 1.$$ (6)

The models input data were obtained from the tasks 1 and 2. In particular, the values of $EPR_{\text{min}}$ and $PR_{\text{max}}$ introduced the acceptable levels of minimal expected portfolio revenue (1) and maximal portfolio risk (2).

Thus, the maximum Markowitz model translated into

$$EPR \rightarrow \max$$ (6)

subject to $W_i \geq S_i$, $i = 1, ..., N$, $\sum_{i=1}^{N} W_i = 1$; (7)

$$PR \leq PR_{\text{max}}.$$ (8)

The minimum Markowitz model looked like

$$PR \rightarrow \min$$ (9)

subject to $W_i \geq S_i$, $i = 1, ..., N$, $\sum_{i=1}^{N} W_i = 1$.

$$EPR \geq EPR_{\text{min}}.$$ (10)

Applications of the formulated Markowitz models under different scenarios can ground the farmers’ strategies on diminishing portfolio risks in times of recession or increasing expected portfolio revenues in times of economic expansion. As such, the calculated shifts in production portfolios will provide the national agricultural authorities with the objective forecasts about country ranks among the world top rivals in cereals and oilseeds markets.

Results and discussion

The described research methodology entailed the relevant empirical outcomes presented in this section.

Global crop portfolios

Hereafter there was intended for wheat, maize, and barley in the group of cereals or for sunflower, soybeans, and rapeseed in the group of oilseeds. To synchronize outcomes of the task 1 with further results referring to Ukraine, the study time frame covered the period of 1996 to 2018 started from launching Ukrainian national currency. It stipulated $T = 23$.

Consistent with Mumey et al. (1992), the presented research examined a portfolio risk in expected revenue. To define the latter, a comprehensive panel data to the task 1 contained yields and farmgate prices for wheat, maize, barley, sunflower, soybeans, and rapeseed by country (FAOStat, 2020). The conducted world comparison considered countries which practice production portfolios and occupy over 1% of the total harvested area under at least 2 crops amongst the analyzed cereals and oilseeds.

As such, Table 1 encompassed 20 countries which were engaged in cereals production portfolios and accumulated 83.1%, 64.3%, and 78.8% of the global farmland under wheat, maize, and barley respectively. Overall, it means a strong commitment of cereals growers to implementing portfolios. Besides, Indonesia, Nigeria, and the Philippines also practiced crop portfolios cultivating 9.6%, 2%, and 2.9% of the total farmland under rice as well as 2.9%, 2.5%, and 1.3% of the world arable land under maize. Similarly, Pakistan occurred to comprise 1.7% of rice and 4.1% of wheat total harvested areas. But given the rice components, the described portfolios were beyond the study focus.
A thorough insight on the indicators in Table 1 revealed different features and priorities of the listed countries. Indeed, China, India, Ethiopia, and Iran are the 1st, 2nd, 12th, and 18th countries by population. In light of providing food security to meet high steady domestic demands, they demonstrated relatively low risks and high absolute revenues. It is also worth mentioning that India and China are the top growers of rice with 26.6% and 18.1% of its total harvested area. In compliance with Rude and An (2015), the largest cereals exporters such as France, Germany, and the USA had moderate portfolio risks paired with average expected portfolio revenues offset by high revenues in absolute terms. The Argentinean, Brazilian, Canadian and Ukrainian portfolio performance appeared to be quiet similar and promising. To some extent, Poland, Romania, Spain and Turkey illustrated opposite priorities in accepting risks justified by higher revenues. In spite of large scale cereals production, Australia, Kazakhstan, and Russia were merged by risky and inefficient results. The worst portfolio performance was found in Algeria and Morocco which should revise their agricultural strategies and improve portfolio indicators of EPR (1), PR (2), and PPR (3).

Table 2 reported data about 10 countries which were involved in oilseeds production portfolios and accumulated 74.6%, 63.1%, and 75.4% of the world harvested areas under sunflower, soybeans, and rapeseed respectively.

Table 2 displayed that the oilseeds portfolio of China dominated over that of India by most indicators. The top world exporters such as France and the USA had similarly balanced oilseeds portfolios. The strongest risk acceptance emerged in Romania that presented an opposite operational priority compared to Canada. The Ukrainian oilseeds portfolio showed better relative indicators of EPR (1) and PR (2) than those in Argentina but, unfortunately, did not gain by PPR (3). As before, despite large occupied farmlands, Kazakhstan and Russia had risky and inefficient oilseeds portfolios in absolute terms.

| Country | Share (%) in the World Farmland under Wheat | Share (%) in the World Farmland under Maize | Share (%) in the World Farmland under Barley | Expected Portfolio Revenue (%) | Portfolio Risk (%) | Present Portfolio Revenue ($/ha) |
|---------|-------------------------------------------|------------------------------------------|--------------------------------------------|-----------------------------|------------------|-------------------------------|
| Algeria | 1.0                                       | 0.0                                       | 2.7                                        | 1.8                         | 29.4             | 581.3                         |
| Argentina | 2.7                                       | 3.7                                       | 2.5                                        | 2.1                         | 22.1             | 801.6                         |
| Australia | 5.1                                       | 0.0                                       | 8.6                                        | 0.2                         | 31.5             | 414.5                         |
| Brazil    | 1.0                                       | 8.3                                       | 0.2                                        | 3.4                         | 22.1             | 765.5                         |
| Canada    | 4.6                                       | 0.7                                       | 5.0                                        | 2.9                         | 23.6             | 693.9                         |
| China     | 11.3                                      | 21.7                                      | 0.8                                        | 1.8                         | 21.6             | 1596.4                        |
| Ethiopia  | 0.8                                       | 1.2                                       | 2.0                                        | 5.5                         | 20.6             | 711.0                         |
| France    | 2.4                                       | 0.7                                       | 3.7                                        | 0.8                         | 21.2             | 1369.0                        |
| Germany   | 1.4                                       | 0.2                                       | 3.4                                        | 0.6                         | 24.3             | 1292.6                        |
| India     | 13.8                                      | 4.7                                       | 1.4                                        | 5.8                         | 14.7             | 906.2                         |
| Iran      | 3.1                                       | 0.1                                       | 3.1                                        | 3.6                         | 13.4             | 704.2                         |
| Kazakhstan | 5.3                                       | 0.1                                       | 5.2                                        | 2.9                         | 41.5             | 151.2                         |
| Morocco   | 1.3                                       | 0.1                                       | 3.3                                        | 2.0                         | 52.0             | 637.6                         |
| Poland    | 1.1                                       | 0.3                                       | 2.0                                        | 0.5                         | 26.4             | 794.9                         |
| Romania   | 1.0                                       | 1.3                                       | 0.9                                        | 5.1                         | 42.5             | 1105.2                        |
| Russia    | 12.3                                      | 1.2                                       | 16.4                                       | 3.0                         | 34.2             | 366.7                         |
| Spain     | 1.0                                       | 0.2                                       | 5.4                                        | 1.6                         | 37.3             | 887.1                         |
| the USA   | 7.5                                       | 17.1                                      | 1.7                                        | 1.4                         | 16.6             | 1209.6                        |
| Turkey    | 3.4                                       | 0.3                                       | 5.4                                        | 1.1                         | 18.6             | 591.9                         |
| Ukraine   | 3.1                                       | 2.4                                       | 5.2                                        | 5.4                         | 26.6             | 785.6                         |

Source: own calculation based on FAOStat (2020)

Table 1: Evaluation of cereals portfolios by top countries.
Revenue forecast

As of 2019, Ukraine ranked the 6th, 3rd, 4th, 1st, 6th, and 3rd among the world top exporters of wheat, maize, barley, sunflower oil, soybeans, and rapeseed. These achievements are essential incentives to delve deeper into improving production portfolios of cereals and oilseeds at the national scope.

The data of six time-series to the task 2 were the revenues (in $ per hectare) from the explored crops delivered by the State Statistics Service of Ukraine (2020) for 1996 to 2019. Hereafter it meant that . The coefficients of the regressions (4) for wheat, maize, barley, sunflower, soybeans, and rapeseed were found by means of the least squares method (5) and assembled in Table 3.

These findings combined and expanded econometric models developed separately for crop prices by Vasylieva (2013) and for yields by Arunachalam and Balakrishnan (2012). As it can be seen from Table 3, all considered cereals and oilseeds had upward revenue trends. The coefficient identified the least annual increase in the revenue for barley and the highest growth in the revenue for rapeseed. Oilseeds appeared to be more uniform by the range of the forecasted revenues for 2020. According to the coefficients \( A_x \), cereals had more stable revenues except for maize. In all cases, the values of R-squared and F-significance permitted applying the forecasted crop revenues to the next stage of this study concerning the optimal production portfolios for cereals and oilseeds in Ukraine.

Portfolio optimization

As mentioned before, the calculations to the task 3 stipulated \( N = 3 \) and \( T = 23 \). Given the biodiversity encouragement, parameters \( S_1, S_2 \) and \( S_3 \) accounted for 0.05 that implied allocating of at least 5% of farmland under each crop in an appropriate portfolio. The conducted calculations were linked with four the most beneficial scenarios. Namely,

- scenario #1 supposed portfolio production with the risk below its current level in Ukraine, to wit, \( PR_{\text{max}} = 0.266 \) for cereals (see Table 1) and \( PR_{\text{max}} = 0.163 \) for oilseeds (see Table 2) in the model (6)-(8);
- scenario #2 addressed portfolio production without restrictions to the risk level, i.e. running the reduced model (6), (7) for both groups of crops in question;
- scenario #3 suggested portfolio production with the expected revenue over its current level in Ukraine, to wit, \( EPR_{\text{min}} = 0.054 \) for cereals (see Table 1) and \( EPR_{\text{min}} = 0.072 \) for oilseeds (see Table 2) in the model (9)-(11);
- scenario #4 defined portfolio production without restrictions to the expected revenue level, i.e. running the reduced model (9), (10) for both groups of crops in question.

The computed figures were aggregated in Tables 4 and 5. Their analysis resulted in the following inferences.
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| Crop      | $A_0$ | $A_1$ | $A_2$ | $A_3$ | $A_4$ | R-squared | F-significance | Revenue Forecast for 2020 ($/ha) |
|-----------|-------|-------|-------|-------|-------|-----------|----------------|----------------------------------|
| Cereals   |       |       |       |       |       |           |                |                                  |
| Wheat     | 95.41 | 23.09 | 60.10 | -0.55 | 1.16  | 0.87      | 0.00           | 658                              |
| Maize     | 52.56 | 42.57 | 135.97| 1.45  | 0.39  | 0.88      | 0.00           | 987                              |
| Barley    | 39.77 | 19.00 | 51.22 | -0.10 | 1.16  | 0.86      | 0.00           | 487                              |
| Oilseeds  |       |       |       |       |       |           |                |                                  |
| Sunflower | -9.29 | 34.51 | 113.88| 1.63  | -0.37 | 0.95      | 0.00           | 744                              |
| Soybeans  | 66.32 | 34.16 | 88.21 | 2.21  | -0.40 | 0.91      | 0.00           | 833                              |
| Rapeseed  | -7.89 | 46.55 | 120.90| 1.33  | -0.37 | 0.94      | 0.00           | 1035                             |

Source: own calculation based on State Statistics Service of Ukraine (2020)

Table 3: Output to regressions on crop revenue.

| Scenario | Share (%) in the World Farmland under | Expected Portfolio Revenue (%) | Portfolio Risk (%) |
|----------|---------------------------------------|-------------------------------|-------------------|
|          | Wheat       | Maize      | Barley        |                 |                 |
| #1       | 35          | 59         | 6             | 5.5             | 26.6            |
| #2       | 5           | 90         | 5             | 5.9             | 30.5            |
| #3       | 30          | 63         | 7             | 5.4             | 26.5            |
| #4       | 25          | 59         | 16            | 4.5             | 24.7            |

Source: own calculation based on State Statistics Service of Ukraine (2020)

Table 4: Optimal portfolios for cereals.

| Scenario | Share (%) in the World Farmland under | Expected Portfolio Revenue (%) | Portfolio Risk (%) |
|----------|---------------------------------------|-------------------------------|-------------------|
|          | Sunflower    | Soybeans   | Rapeseed       |                 |                 |
| #1       | 38          | 5          | 57             | 7.4             | 16.3            |
| #2       | 5           | 5          | 90             | 7.8             | 22.4            |
| #3       | 47          | 5          | 48             | 7.2             | 15.4            |
| #4       | 48          | 21         | 31             | 6.8             | 14.5            |

Source: own calculation based on State Statistics Service of Ukraine (2020)

Table 5: Optimal portfolios for oilseeds.

Firstly, both cereals and oilseeds portfolios derived from the scenarios #2 gravitated to more specialized productions. According to Czyzewski and Smedzik-Ambrozy (2015), similar farmers’ strategies may be explained by shifting to the crops with larger revenues, reduced technological costs, and diminished marketing expenditures through the deteriorated biodiversity.

Secondly, both cereals and oilseeds portfolios derived from the scenarios #4 fostered more diversified productions driven by the farmers’ strategic priority to mitigate natural and marketing risks (Lin, 2011).

Thirdly, under scenarios #1 and #3 Ukraine retained its positions by EPR and PR ranked 3rd and 13th for cereals (see Tables 1 and 4) as well as ranked 3rd twice for oilseeds (see Tables 2 and 5). Scenario #2 applied to cereals elevated Ukrainian EPR up to 1st rank but decreased its PR by 1 position. Scenario #4 acted the opposite way. It dropped Ukrainian EPR to 4th rank but lifted its PR up to 10th rank. Under scenarios #2 and #4 Ukrainian ranks for oilseeds were constant by EPR but shifted to 8th and 2nd by PR.

Finally, according to PPR Ukrainian portfolio revenues were relatively low in absolute terms ranked 10th out of 20 countries by cereals and 7th out of 10 countries by oilseeds. Sure enough, Ukrainian farmers are price-takers in the global scale and can not influence a marketing risk (Velychko et al., 2019). Nevertheless, it is an unfavorable but not a hopeless situation.
Ukrainian farmers are able to increase their yields of cereals and oilseeds to reach the levels of the most advanced producers via improved technologies and implemented innovations (Vasylieva and Pugach, 2017). As such, the national agricultural authorities ought to encourage this activity and incentivize biodiversity through the political measures of the permissible financial protection of the domestic cereals and oilseeds growers.

Conclusion

In sum, the largest portfolio producers cultivate 341 million hectares or 74.7% of the world farmland under wheat, maize, and barley and 127 million hectares or 67.1% of the total harvested areas under sunflower, soybeans, and rapeseed. These crops are a cornerstone in providing food, feed and bio-fuel resources. Markowitz indicators unfolded that the top cereals producers were more numerous and less uniform compared to the top oilseeds growers. The latter ones practiced less risky activity with higher expected portfolio revenues. The research insight also revealed that Argentina, Canada, China, France, India, Kazakhstan, Romania, Russia, the USA, and Ukraine run large scale portfolios by both cereals and oilseeds. As of 2019, their combined cultivated area amounted to 388.9 million hectares or 60.2% of the world farmland under these crops.

A combination of econometric and optimization models appeared to be a relevant mathematical technique to enhance portfolio performance by the world major field crops at a country level. It made possible to alleviate uncertainty in yields and prices triggered by natural and marketing risks intrinsic to agribusiness. The proposed utilization of Markowitz models delivered options on reasonable farmland allocation and biodiversity promotion which are global imperatives of contemporary agriculture. With regard to Ukrainian circumstances, the conducted calculations detected opportunities to decrease portfolio risks and raise expected portfolio revenues for the considered crops.

Taking into account the annual revenue fluctuations in cereals and oilseeds markets, the recommended portfolios need regular updates and amendments that can define a promising avenue for further scientific elaborations.

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