Star Formation and Stellar Mass Assembly in Dark Matter Halos: From Giants to Dwarfs

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\textbf{ABSTRACT}

The empirical model of Lu et al. (2014) is updated with recent data and used to study galaxy star formation and assembly histories. At \(z > 2\), the predicted galaxy stellar mass functions are steep, and a significant amount of star formation is hosted by low-mass haloes that may be missed in current observations. Most of the stars in cluster centrals formed earlier than \(z \approx 2\) but have been assembled much later. Milky Way mass galaxies have had on-going star formation without significant mergers since \(z \approx 2\), and are thus free of significant (classic) bulges produced by major mergers. In massive clusters, stars bound in galaxies and scattered in the halo form a homogeneous population that is old and with solar metallicity. In contrast, in Milky Way mass systems the two components form two distinct populations, with halo stars being older and poorer in metals by a factor of \(\approx 3\). Dwarf galaxies in haloes with \(M_h < 10^{11}h^{-1}M_\odot\) have experienced a star formation burst accompanied by major mergers at \(z > 2\), followed by a nearly constant star formation rate after \(z = 1\). The early burst leaves a significant old stellar population that is distributed in spheroids.

\textbf{Key words:} galaxies: haloes — galaxies: formation — dark matter — methods: statistical

\section{INTRODUCTION}

In the current cold dark matter (CDM) paradigm, galaxies are assumed to form and evolve in extended dark matter haloes (see Mo, van den Bosch & White 2010 for an extensive review). Over the years, it has become clear that the star formation and stellar mass assembly histories of galaxies are very different from the mass assembly histories of their dark matter haloes. Theoretical modelling and $N$-body simulations have shown that CDM haloes form in a hierarchical fashion, with smaller haloes forming earlier than the more massive ones (e.g., van den Bosch 2002, Zhao et al. 2003). In contrast, the star formation histories (SFHs) of galaxies indicate that more massive galaxies, which typically reside in more massive haloes, form their stars earlier. This “downsizing” behaviour is inferred from both the archaeological record of their stellar populations (Heavens et al. 2004, Gallazzi et al. 2005, Panter et al. 2007) and from the specific star formation rates of galaxies as a function of stellar mass and redshift (e.g., Noeske et al. 2007a,b, Leitner 2012). However, because of the flux limits that hamper galaxy surveys, these results are mainly valid for relatively bright/massive galaxies. Only recently has it become possible to infer the star formation histories (SFHs) of nearby, isolated dwarf galaxies ($M_\star < 10^8M_\odot$) using the colour-magnitude diagram (CMD) of resolved stars (Weisz et al. 2011, 2013). The data indicate that these dwarfs contain a significant amount ($\sim 50\%$ in stellar mass) of old stars, suggesting that the “downsizing” trend may reverse for dwarf galaxies. Dwarf galaxies and more massive massive galaxies, which typically reside in more massive haloes, form their stars earlier. This “downsizing” behaviour is inferred from both the archaeological record of their stellar populations (Heavens et al. 2004, Gallazzi et al. 2005, Panter et al. 2007) and from the specific star formation rates of galaxies as a function of stellar mass and redshift (e.g., Noeske et al. 2007a,b, Leitner 2012). However, because of the flux limits that hamper galaxy surveys, these results are mainly valid for relatively bright/massive galaxies. Only recently has it become possible to infer the star formation histories (SFHs) of nearby, isolated dwarf galaxies ($M_\star < 10^8M_\odot$) using the colour-magnitude diagram (CMD) of resolved stars (Weisz et al. 2011, 2013). The data indicate that these dwarfs contain a significant amount ($\sim 50\%$ in stellar mass) of old stars, suggesting that the “downsizing” trend may reverse for dwarf galaxies. Dwarf galaxies and more massive

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samples spanning more than 5 orders of magnitude in stellar mass (10^7 M_⊙ - 10^{12} M_⊙) are expected to provide important constraints on galaxy formation and evolution.

In general, a galaxy can grow its stellar mass either via in situ star formation or by accreting other galaxies (i.e., ‘merging’ or ‘galactic cannibalism’). The relative importance of these two distinct acquisition processes is likely to play an essential role in shaping the morphology of a galaxy and to increase the diversity of the galaxy population. Indeed, it is generally believed that the disks of spiral galaxies form through the cooling and collapse of gas into a rotationally supported, gaseous disk that forms most of its mass of in situ star formation. This is strongly supported, e.g., by Kauffmann et al. (1993). For present day elliptical galaxies, the most popular scenario is that they form through major mergers of disk galaxies (Toomre & Toomre 1972).

Given that the hierarchical formation of dark matter haloes is the backbone of galaxy formation, and given that dark matter is the dominant mass component in the Universe, understanding the origin and diversity of the galaxy population requires a solid understanding of the connection between galaxies and dark matter haloes. The last decade has seen tremendous progress in this area, largely owing to the development of numerous statistical techniques to infer the galaxy-dark matter halo connection. These include galaxy clustering (e.g., Jing, Mo & Kaise 1998; Mo et al. 1999; Yang et al. 2003), van den Bosch et al. 2004), Conroy et al. 2007; Norberg et al. 2008), More et al. 2009, 2011), galaxy group catalogs (Yang et al. 2005; Weinmann et al. 2006), sub-halo abundance matching (e.g., Vale & Ostriker 2004; Conroy et al. 2009; Moster et al. 2010; Behroozi et al. 2010), and combinations thereof (e.g., Cacciato et al. 2009; Li et al. 2009; Cacciato et al. 2013; Leauthaud et al. 2012a; Mandelbaum et al. 2013).

By combining the galaxy-dark matter connection as a function of redshift with halo merger trees, which describe the hierarchical assembly of dark matter haloes, one obtains a statistical description of how galaxies assemble their stellar mass over time. Such an ‘empirical’ approach is intuitive and transparent in that it describes galaxy evolution within the natural framework of hierarchical structure formation. This method was pioneered by Conroy et al. (2007, 2009) and Yang et al. (2009), and has since been applied in numerous studies (e.g., Moster et al. 2010; 2013; Behroozi et al. 2010; 2013a; Avila-Reese & Firmani 2011; Yang et al. 2012; 2013; Yang et al. 2013; Behroozi et al. 2013). An important new insight that has resulted from this ‘empirical modelling’ approach is that there is an amazing amount of ‘regularity’ and ‘simplicity’ in galaxy demographics. In particular, the relatively mild evolution in the M_⋆ - M_h relation with redshift is found to translate into an instantaneous star formation efficiency (i.e., the star formation rate divided by the baryon accretion rate) that peaks at a characteristic halo mass of ∼ 10^{12} h^{-1} M_⊙ over the entire epoch from z = 8 to the present day, and almost all star formation has occurred inside haloes that lie within the narrow range 10^{11} h^{-1} M_⊙ ≤ M_h ≤ 10^{12} h^{-1} M_⊙ (Yang et al. 2012; 2013; Leauthaud et al. 2012a,b; Behroozi et al. 2013a,b; Moster et al. 2013). In addition, these studies have shown that virtually all stellar mass is assembled in situ: merging is only a significant channel for mass assembly for the most massive galaxies. In what follows we will refer to this picture of galaxy formation as the ‘Slow-Evolution’ model, to emphasise that it suggests little evolution in the halo mass dependence of the star formation efficiency. A recent study by the authors (Lu et al. 2014) has argued for an important revision of this ‘Slow-Evolution’ picture. Using data on the faint-end of the luminosity function of cluster galaxies, they show that low mass haloes (M_h ≤ 10^{11} h^{-1} M_⊙) have to form stars efficiently, but only at high redshift (z ≥ 2). In particular, they identified z ≃ 2 or 3 as a new characteristic epoch in galaxy formation, where there is a sudden transition in the star formation efficiency of low mass haloes. This transition leads to some interesting predictions, e.g., a significant old stellar population in present-day dwarf galaxies with M_h ≤ 10^8 h^{-2} M_⊙ and shallow slopes at high redshift of the galaxy stellar mass and star formation rate functions. Interestingly, recent work based on deeper high redshift surveys provide some evidence for such a steepening. In this paper, we use the model of Lu et al. (2014) updated with more recent observational data to characterise in detail the star formation and assembly histories of galaxies across cosmic time, addressing questions related to in situ star formation versus accretion, downsizing in both star formation and assembly, mergers of galaxies and their roles in shaping galaxy morphology, and the prevalence of halo stars. Wherever possible we will contrast the differences between the ‘Slow-Evolution’ model and the modified picture advocated by Lu et al. (2014).

This paper is organised as follows. Our method to model the star formation-halo mass connection is described in §2. The overall trends in the star formation and assembly histories are described in §3. In §4 we describe the total star formation and assembly histories as a function of halo (stellar) mass, paying particular attention to in situ star formation versus accretion, the breakdown of downsizing, and the global star formation rate density in connection to the ionisation state of the Universe. In §5 we focus on galaxy merger rates and their implications for the morphological transformation of galaxies. In §6 we address the stellar populations of galaxies as function of their stellar mass, paying particular attention to the properties of halo stars. Finally, we summarise our results in §7. Throughout the paper, we use a ΛCDM cosmology.
ogy with $\Omega_{m,0} = 0.273$, $\Omega_{\Lambda,0} = 0.727$, $\Omega_b,0 = 0.0455$, $h = 0.704$, $n = 0.967$ and $\sigma_8 = 0.811$. This set of parameters is from the seven year WMAP observations (Komatsu et al. 2011). In addition, unless stated otherwise, we adopt the stellar population synthesis model of Bruzual & Charlot (2003) and a Chabrier (2003) IMF.

2 THE EMPIRICAL MODEL OF STAR FORMATION IN DARK MATTER HALOS

2.1 The Model

In this section we provide a brief description of the model of Lu et al. (2014), which we adopt here to make model predictions, referring the reader to the original paper for details.

The hierarchical assembly of individual dark matter haloes is modelled using halo merger trees generated with the Monte-Carlo model of Parkinson et al. (2008), which is based on a modified treatment of the extended Press-Schechter formalism calibrated with $N$-body simulations (see Cole et al. 2008). As shown in Jiang & van den Bosch (2014), the merger trees obtained with this method are as accurate as those obtained from high-resolution $N$-body simulations.

The star formation rate (SFR) of a central galaxy in a halo at a given redshift $z$ is assumed to be determined by the virial mass of the host halo, $M_h(z)$, and the redshift $z$, so that we can write

\[
SFR = M_\star [M_h, z],
\]

where $M_\star = M_\star(z)$ is the instantaneous halo mass. Lu et al. (2014) adopted the following functional form for the mass and redshift dependence:

\[
M_\star = \frac{E}{\tau} (M_\star / M_\odot) (X + 1)^{\alpha} \left(\frac{X + \bar{R}}{X + 1}\right)^{\beta} \left(\frac{X_0 + \bar{R}}{X + \bar{R}}\right)^{\gamma},
\]

where $E$ is a free parameter that sets the overall efficiency; $f_b = M_{b,0}/M_{h,0}$ is the cosmic baryon mass fraction; and $\tau = (1/10H_0) (1 + z)^{-3/2}$ roughly describes the dynamical timescale of haloes at redshift $z$. We define the quantity $X$ as $X \equiv M_h/M_c$, where $M_c$ is a characteristic mass; and $\bar{R}$ is a positive number smaller than 1. Hence, the SFR depends on halo mass through a piece-wise power law, with $\alpha$, $\beta$, and $\gamma$ being the three power indices in the three mass ranges separated by the two characteristic masses, $M_c$ and $\bar{R}M_c$.

The stellar mass can be obtained by going through the merger trees and integrating the SFR with the assumed stellar evolution model (Bruzual & Charlot 2003) and IMF (Chabrier 2003). To get the luminosities, we use the metallicity - stellar mass relation from Gallazzi et al. (2005). Note that the $z$ band and $r$ band luminosities are quite insensitive to the assumed metallicity.

Lu et al. (2014) considered three different models. In Model I they assumed that all the model parameters were independent of redshift. However, they showed that such a model was unable to match simultaneously the observed galaxy stellar mass functions (SMFs) in the redshift range between $z = 0$ and $z = 4$. This can be remedied by allowing $\alpha$ to depend on redshift according to

\[
\alpha = \alpha_0 (1 + z)^{\alpha'},
\]

with both $\alpha_0$ and $\alpha'$ being free parameters. This Model II is able to fit the SMFs from $z = 0$ to $z = 4$, and is very similar to the ‘Slow Evolution’ model discussed above; virtually all stars form in dark matter haloes in a narrow band of halo mass: $10^{11} h^{-1} M_\odot \lesssim M_h \lesssim 10^{12} h^{-1} M_\odot$. However, this model is unable to match the steep, faint-end upturn of the cluster galaxy luminosity function at $z = 0$ (Pope et al. 2006). This upturn requires an additional modification, namely that the parameter $\gamma$, which controls the star formation efficiency in low mass haloes, depends on redshift according to

\[
\gamma = \begin{cases} 
\gamma_a & \text{if } z < z_c \\
\left(\frac{\gamma_a - \gamma_b}{z + 1}\right) + \gamma_b & \text{otherwise},
\end{cases}
\]

so that it changes from $\gamma_a$ at high-$z$ to $\gamma_b$ at low-$z$, with a transition redshift $z_c$. Performing a Bayesian inference using both the stellar mass functions from $z = 0$ to $z = 4$ and the cluster galaxy luminosity function as data constraints, Lu et al. (2014) obtained a model, Model III, that fits all the data. This model differs from the ‘Slow Evolution’ model (and thus Model II) in that it predicts efficient star formation in low mass haloes ($M_h \lesssim 10^{11} h^{-1} M_\odot$) but only for $z > z_c \approx 2$. As we will see later, the value of $z_c$ is quite well constrained. Our tests using a simpler model with $z_c = 0$, shows that the model given by equation (1) is favourably by a factor $K \approx e^{15}$ in terms of the Bayes ratio [see equation (19) in Lu et al. (2014) for the definition], demonstrating clearly that the data prefer a non-zero $z_c$.

The above SFR model is only valid for central galaxies, i.e., galaxies that reside at the centres of their dark matter host haloes, where they act as the recipients of any new gas that looses its binding energy. Motivated by the notion that galaxies quench their star formation once they become satellite galaxies (e.g., Balogh et al. 2000; van den Bosch et al. 2008; Wetzel et al. 2012), Lu et al. (2014) model the SFR of satellite galaxies using a simple $\tau$ model:

\[
M_{\star, sat}(t) = M_{\star}(t_s) \exp\left(-\frac{t - t_s}{\tau_{sat}}\right),
\]

where $t_s$ is the time when the satellite is accreted into its host and $M_{\star}(t_s)$ is the SFR of the satellite galaxy at $t = t_s$. The quantity $\tau_{sat}$ is the ‘quenching’ time scale for satellite galaxies, which is modelled as

\[
\tau_{sat} = \tau_{sat,0} \exp\left(\frac{M_r}{M_{c,r}}\right),
\]

where $\tau_{sat,0}$ is the exponential decay time for a satellite galaxy with a stellar mass of $M_{c,r}$; both $\tau_{sat,0}$ and $M_{c,r}$ are treated as free parameters. As discussed in Lu et al. (2014), the choice of $\tau_{sat}$ is motivated by the fact that a decreasing quenching time scale with stellar mass seems to be required by the data.
Table 1. The constrained model parameters of Model II, in terms of the means and the variances. The observational constraints used are listed in the first row. B12 is for Baldry et al. (2012), S12 for Santini et al. (2012) and T14 for Tomczak et al. (2014). \( M_\star \) is in units of \( 10^{10} h^{-1} M_\odot \), and \( M_{\ast,e} \) is in units of \( 10^{10} h^{-2} M_\odot \).

| Parameter | \( \text{mean}\pm\sigma \) | \( \text{mean}\pm\sigma \) |
|-----------|----------------|----------------|
| \( \alpha_0 \) | \(-3.7\pm0.82\) | \(-3.4\pm0.84\) |
| \( \alpha' \) | \(-0.46\pm0.11\) | \(-0.45\pm0.11\) |
| \( \beta \) | \(3.4\pm0.86\) | \(2.6\pm0.99\) |
| \( \gamma \) | \(0.89\pm0.63\) | \(1.3\pm0.77\) |
| \( \log_{10}(M_\star) \) | \(1.7\pm0.13\) | \(1.8\pm0.18\) |
| \( \log_{10}(R) \) | \(-1.1\pm0.34\) | \(-1.1\pm0.45\) |
| \( \log_{10}(\mathcal{E}) \) | \(0.30\pm0.27\) | \(0.017\pm0.27\) |
| \( \log_{10}(H_0\tau_{9,0}) \) | \(-0.98\pm0.17\) | \(-0.85\pm0.13\) |
| \( \log_{10}(M_{\ast,e}) \) | \(0.81\pm0.42\) | \(0.84\pm0.38\) |
| \( f_{TS} \) | \(0.36\pm0.17\) | \(0.38\pm0.15\) |

2.2 Updating model parameters with recent observational data

In Lu et al. (2014) two sets of observational data were used to constrain the models described above. One is the galaxy SMFs at different redshifts and the other is the \( z \)-band cluster galaxy luminosity function from Popesso et al. (2006). The SMFs are those from Baldry et al. (2012) for \( z \approx 0 \), from Perez-Gonzalez et al. (2008) for \( 1.0 < z < 1.3 \), from Marchesini et al. (2009) for \( 2.0 < z < 3.0 \), and from Stark et al. (2009) for \( 3.19 < z < 4.73 \). The results presented in Lu et al. (2014) are based on Model II constrained by the SMFs alone and Model III constrained by both the SMFs and the cluster galaxy luminosity function. As mentioned above, Model II is unable to match the steep, faint-end upturn observed in the cluster galaxy luminosity function.

As shown in Lu et al. (2014), one way to distinguish Model II and Model III is the difference in their predicted faint-end slope of the SMF at high redshift.

The SMF predicted by Model II is quite flat at the low-mass end at all redshifts, while Model III predicts a steepening of the SMF at the low-mass end at high \( z \). More recently, analyses based on deeper surveys provide some evidence for such a steepening. It is, therefore, interesting to use the new data to update our model parameters. In this paper we use two sets of SMFs recently published. The first is that of Santini et al. (2012) based on the Early Release Science (ERS) data of the Wide Field Camera 3 (WFC3) in the GOODS-S Field, and the SMFs for galaxies in the redshift range between 0.6 and 4.5 are estimated to a stellar mass limit of a few times \( 10^{10} M_\odot \). The second set is that of Tomczak et al. (2014), who estimated the galaxy SMFs in the redshift range 0.2 - 3.0 using data from the FourStar Galaxy Evolution Survey (ZFOURGE) and the Cosmic Assembly Near-IR Deep Extragalactic Legacy Survey (CANDELS). Unfortunately, the two sets are not completely consistent with each other. While at \( z < 2.0 \) the results obtained by both are similar, at \( z > 2.0 \) the SMFs at the low-mass ends obtained by Tomczak et al. (2014) are lower than those obtained by Santini et al. (2012) by a factor of 2. In the present paper we use the two sets of data separately to update our model parameters, and to check the reliability of our results against uncertainties in the observational data.

In practice, we replace the SMFs at \( z > 1 \) in Lu et al. (2014) with the new SMFs to constrain the models. As in Lu et al. (2014), we use the MULTI-NEST method developed by Perez et al. (2009), which implements the nested sampling algorithm of Skilling (2006), to explore the model parameter space and to make posterior predictions. The details of the method
and implementations can be found in Lu et al. (2014) and will not be repeated here. The new inferences of the model parameters are shown in Table 1 for Model II and in Table 2 for Model III. The comparison between the posterior predictions and the constraining data is shown in Figures 1 and 2. We find that without the cluster data the new data sets alone cannot distinguish decisively between Model II and Model III, because at \( z \geq 1 \), the posterior predictions and the constraining data is shown in Figures 1 and 2. We find that without the cluster data the new data sets alone cannot distinguish decisively between Model II and Model III, because at \( z > 3 \), the new SMFs are only complete for \( M_*>3 \times 10^9 M_\odot \), where the two models are quite similar. The model inferences based on the Santini et al. (2012) data are similar to those obtained in Lu et al. (2014). The inferences from Tomczak et al. (2014) data are qualitatively the same, except that the inferred star formation rates at \( z > 3 \) in low-mass haloes are lower by a factor of \( \sim 2 \). Note that both models over-predict slightly the SMF in the intermediate redshift range, and even Model III under-predicts the cluster galaxy luminosity function at the faint end somewhat, indicating that either the faint end slope in the cluster galaxy luminosity function is overestimated, or the SMF is under-estimated in the intermediate redshift range, or our Model III is still not flexible enough to match the details of the data.

Figure 3 demonstrates the major differences between Model II and Model III. The upper panels show the SMFs and \( M_*/M_\odot \) at different redshifts predicted by Model II constrained by the \( z \approx 0 \) SMF of Baldry et al. (2012) together with the SMFs of Santini et al. (2012) at \( z > 1 \). The solid lines in the lower panels show the predictions of Model III constrained by the \( z \approx 0 \) SMF of Baldry et al. (2012), the SMFs of Santini et al. (2012) at \( z > 1 \), and the cluster galaxy luminosity function of Popesso et al. (2009). As found in Lu et al. (2014), the main difference between Model II and Model III lies in the predicted faint end, especially at high redshift. For comparison, the dashed lines in the lower panels show the predictions of Model III but constrained with the SMFs of Tomczak et al. (2014).

The model constrained by the Santini et al. (2012) data predicts systematically higher and steeper SMFs at \( z \geq 3 \) than that constrained by Tomczak et al. (2012). The red curves (best fit) and the bands (95% credible intervals) are predictions of Model III, while the green curves are the predicted means of Model II.
3 GENERAL TRENDS AND CHARACTERISTIC SCALES

To characterise the general properties of the in situ star formation in different haloes at different redshift, we define a star formation efficiency for a halo as the ratio between the in situ SFR in the central galaxy and the mean halo mass accretion rate $\dot{M}_h(z)$ multiplied by the universal baryon fraction $f_B$:

$$\epsilon_{\text{SFR}}(z) \equiv \frac{\text{SFR}(z)}{f_B \dot{M}_h(z)}.$$  \hspace{1cm} (7)$$

We define the halo mass accretion rate as

$$\dot{M}_h \equiv [M_h(t) - M_{\text{main}}(t - dt)]/dt,$$ \hspace{1cm} (8)

where $M_{\text{main}}$ is the mass of the main progenitor. The plots in Figure 4 show $\epsilon_{\text{SFR}}$ as a function of $M_h(z)$ and $z$. As one can see, Model II predicts that the in situ
Figure 4. Star formation efficiency and merger rate in the halo mass - redshift plane. The blue shading is the star formation efficiency as indicated in the colour bar on the right. The blue solid lines correspond to star formation efficiency 0.1 (inner two lines) and 0.03 (outer lines). The solid red lines are the loci of one merger event per Hubble time, with the hedged sides corresponding to a higher merger frequency. The left panels are for major mergers (with mass ratios larger than $1/3$) and the right panels are for minor mergers with mass ratios between $1/10$ and $1/3$. The solid grey lines are the mean mass assembly histories of dark matter haloes with present-day masses equal to $10^{11}, 10^{12}, \cdots, 10^{15} M_{\odot}$. The upper panels are predictions of Model II and the lower panels are the predictions of Model III.

Star formation is most efficient (with $\epsilon_{\text{SFR}} > 0.3$) in a narrow band between $10^{11} h^{-1} M_{\odot}$ and $10^{12} h^{-1} M_{\odot}$, with a tilt towards lower mass haloes at lower redshifts. Outside the band, the star formation efficiency drops rapidly towards both higher and lower masses without depending strongly on redshift. This trend of star formation efficiency with halo mass and redshift agrees with the results obtained earlier by Bouche et al. (2010), Behroozi et al. (2013b), Bethermin et al. (2013), Tacchella et al. (2013), and Yang et al. (2013), using different constraints and methods. Model III predicts a similar trend except for haloes with masses $< 10^{11} h^{-1} M_{\odot}$. Instead of a strong suppression of star formation with decreasing halo mass, the star formation efficiency remains $\sim 1/30$ at $z > 3$ for all $M_h < 10^{11} h^{-1} M_{\odot}$ haloes.

For central galaxies, another potentially important process that can affect its stellar mass is the accretion of satellites. A satellite may sink and merge with the central galaxy owing to dynamical friction, adding stars to the central, and perhaps also changing its size and morphology. To characterise this process, we calculate the mean galaxy merger rate for haloes of a given mass at a given redshift. We distinguish two different types of mergers: (i) major mergers in which the stellar mass ratio between the merging satellite and the central galaxy is $\geq 1/3$ and (ii) minor mergers in which the secondary to primary mass ratio is between $1/10$ and $1/3$. When calculate the mass ratios, we use the original stellar mass of the satellites before they deposit a fraction $1 - f_{\text{TS}}$ into the stellar halo component. This choice is discussed in the end paragraph of §5. We define the merger rate as the number of mergers per unit time multiplied by the Hubble time $t_{\text{H}}(z) \equiv H(z)^{-1}$. In Figure 4 the red lines are the loci of one merger event per $t_{\text{H}}(z)$ in the halo mass - redshift plane; haloes on the hedged sides of the loci on average have more than one merger per
$t_H(z)$. We show results for both major (left panels) and minor (right panels) mergers, and separately for Model II (upper panels) and Model III (lower panels).

For Model II, central galaxies at $z = 0$ have experienced at least one major merger per Hubble time if they are hosted by haloes with masses larger than $\approx 10^{13} h^{-1} M_\odot$. At $z > 1$, frequent major mergers only occur for centrals hosted by haloes with masses higher than $\sim 3 \times 10^{12} h^{-1} M_\odot$. The predictions of Model III are quite similar for massive haloes, but an additional branch of high major merger rate is also predicted for low mass haloes ($10^{10} h^{-1} M_\odot < M_h < 10^{11} h^{-1} M_\odot$) at $z > 3$. For such redshifts and halo masses, the stellar mass predicted by Model III for the central galaxy is roughly proportional to the halo mass, and mergers of galaxies with comparable stellar masses are more likely to occur.

Comparing the red hedged lines indicating mergers and the star formation efficiency, one can see that most galaxies with high star formation efficiency are not connected with the major mergers of galaxies. In Model II, only central galaxies in haloes with $M_h = 10^{13.2} - 10^{13.9} h^{-1} M_\odot$ at $z > 2$ have both a relatively high star formation efficiency and a high frequency of major mergers. In Model III, in addition to these massive systems, central galaxies in low-mass haloes with $M_h = 10^{10} - 10^{11} h^{-1} M_\odot$ at $z > 3$ can also experience major mergers while actively forming stars. Thus, major merger triggered star formation cannot play an important role in regulating star formation for the majority of star forming galaxies at any redshift. More galaxies can experience minor mergers while actively forming stars, as shown in the right panels. In particular, Model III predicts that active star forming central galaxies in all haloes with $M_h > 10^{10} h^{-1} M_\odot$ may have experienced minor mergers at $z > 2$. Thus, minor mergers could in principle affect star formation at $z > 2$ but not at lower redshifts.

The following set of functions and scales characterise the star formation efficiency and merger frequency:

- The ridge of the highest star formation efficiency is well described by
  \[ M_h(z) \approx 3 \times 10^{13} h^{-1} M_\odot (1 + z)^{0.3}, \]
  with a height $\epsilon_{\text{mx}} \sim 0.5$ and a FWHM $\Delta \log_{10}(M_h) \approx 1.0$.

- The line separating frequent from infrequent major mergers for massive haloes can be approximated by
  \[ M_h(z) \approx 10^{13} h^{-1} M_\odot [0.7 \exp(-z/0.6) + 0.3]. \]

- The line separating frequent from infrequent minor mergers in the entire redshift range for Model II, and at $z < 2$ for Model III, can be approximated by
  \[ M_h(z) \approx 10^{13} h^{-1} M_\odot [\exp(-z/0.8) + 0.06]. \]

- For Model-III, there is a characteristic redshift, $z_c \sim 2$, above which the star formation efficiency and the major merger frequency are boosted in low mass haloes with $M_h(z) \lesssim 10^{11} h^{-1} M_\odot$, and the minor merger frequency is boosted in all haloes with $M_h(z) > 10^{10} h^{-1} M_\odot$.

Over plotted on these plots are the mean mass assembly histories of dark matter haloes, which have been obtained by averaging over the main branches of the merger trees. Together with the star formation efficiency and the loci of merger rates, they provide a crude picture of how galaxies go through different stages in star formation and stellar mass acquisition as their host haloes grow with time, as we describe in detail in the following sections.

4 STAR FORMATION AND STELLAR MASS ASSEMBLY HISTORIES

4.1 Star formation histories

Following a galaxy merger tree, when two galaxies merge, the total SFH of the remnant is simply the weighted sum of the SFHs of the two progenitors,

\[ \text{SFR}_{\text{rem}}(t) = \sum_{i=1,2} \omega_i \text{SFR}_i(t), \]

where $\omega_i = 1$ for the progenitor that is the central and $\omega_i = f_{\text{FS}}$ for the satellite. The $t$ in the parentheses denotes the time steps just before the merger. This total SFH, which takes into account the history of the accreted stars, is needed when modelling the stellar population of the galaxy. In Figure 6 the black solid lines show the total SFHs of central galaxies in different dark halo mass ranges by averaging over a large number of halo merger histories using the best fit parameters. For comparison, the shaded band in each panel represents the variance among different merger

Figure 6. The fraction of stars formed \textit{in situ} in present day central galaxies of haloes with different masses. Shown are the predictions of Model II (green) and Model III (red). The curves are the averages obtained from an ensemble of halo merger trees, while the shaded areas represent the variances among the different halo merger trees.

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trees of the final halo mass in question. We show results for both Model II (upper panels) and Model-III (lower panels) and for five final halo masses, as indicated in each of the panels. This plot is similar to that already shown in [Lu et al. (2014)], except that there the focus is on the inference uncertainty while here the focus is on the variance owing to different halo merger histories. We note that the variance among different halo merger trees is quite large, particularly for low-mass haloes, and is in general much larger than the variance owing to inference uncertainties in model parameters constrained by the present data.

It is clear that haloes of different present-day masses have different star formation histories. For centrals in massive clusters with $M_h(z=0) \sim 5 \times 10^{14} h^{-1} M_\odot$, the SFR peaks at $z \approx 3$ and the majority of the stars form in a narrow time range, which is about 10 Gyrs ago ($z > 2$). In contrast, for Milky-Way mass haloes, the star formation rate reaches a maximum between $z = 2$ and $z = 1$ and decreases only mildly to the present day. For dwarf galaxies in haloes with $M_h(z=0) < 10^{11} h^{-1} M_\odot$, the predictions of Model II and Model III are significantly different. For model II, most stars in these dwarf galaxies formed

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**Figure 5.** The star formation histories in haloes with different present-day masses (as indicated in the upper panels) predicted by the best-fit parameters of Model II (upper panels) and Model III (lower panels). The thick solid lines are the averages; the shaded areas are the 95% ranges of variance owing to different halo merger histories. The dashed black lines are the average differential assembly histories.

**Figure 7.** The distribution of the redshift, $z_f$, at which 50% and 10% of the stars in a central galaxy have formed (green contours) and have assembled (red contours). We show results for haloes with five masses at $z = 0$, as indicated. The upper panels are the predictions of Model II, while the lower panels are for Model III.
The stars observed in a galaxy can come from both in situ star formation and the accretion of stars that formed earlier in its progenitors. In addition, stars also evolve with time, and the mass in stars can change owing to stellar winds and supernova explosions. Taking all these into account, the stellar mass in a galaxy at redshift $z$ can be written as

$$M_*(z) = \int \text{SFR}_{\text{insitu}}(t')R\left[t-t'\right] dt' + \sum_s \int f_{\text{TS}}M_*(t_s; t) \mathcal{H}(t-t_s-\tau_{\text{merg}}) dt$$

where $R(\tau)$ is the fraction of initial mass that is still in stars for a stellar population with an age of $\tau$, $M_*(t_s; t)$ is the stellar mass at time $t$ of a satellite accreted at time $t_s$, and $\tau_{\text{merg}}$ is the dynamical friction time scale of the satellite used to model the time it takes for the satellite to merge with the central after $t_s$. The function, $\mathcal{H}(x) = 1$ if $x > 0$ and $\mathcal{H}(x) = 0$ otherwise, is used to ensure that only satellites that can sink to the centre and merge with the primary contribute to the mass of the primary. The summation is over all satellites accreted into the host halo. In practice, the stellar mass of a galaxy is recorded in a number of time bins so that the addition of stellar mass owing to accretion is done separately for individual bins. Following Lu et al. (2014), we estimate the value of $R(\tau)$ from the spectral synthesis model of Bruzual & Charlot (2003) assuming a Chabrier IMF.

The average differential assembly histories obtained in this way are shown in Figure 6 as the dashed lines. For both dwarf and Milky-Way sized galaxies, the stellar mass assembly histories are almost parallel to the SFHs except at the beginning of star formation. The difference in amplitude, which is about a factor of 2, owes to the mass loss of evolved stars. This suggests that the assembly of such galaxies is dominated by in situ star formation, rather than by the accretion of stars formed in progenitors. We will have a more detailed discussion about this in the following subsection. For massive cluster galaxies, the assembly histories start with a strong episode of in situ star formation at $z > 2$, which is followed by a long period of mass accretion at roughly a constant rate.

### 4.2 Stellar mass assembly histories

The stellar mass assembly history of a galaxy describes how the stellar mass in the galaxy changes with time. The stars observed in a galaxy can come from both in situ star formation and the accretion of stars that formed earlier in its progenitors. In addition, stars also evolve with time, and the mass in stars can change owing to stellar winds and supernova explosions. Taking all these into account, the stellar mass in a galaxy at redshift $z$ can be written as

$$M_*(z) = \int \text{SFR}_{\text{insitu}}(t')R\left[t-t'\right] dt' + \sum_s \int f_{\text{TS}}M_*(t_s; t) \mathcal{H}(t-t_s-\tau_{\text{merg}}) dt$$

where $R(\tau)$ is the fraction of initial mass that is still in stars for a stellar population with an age of $\tau$, $M_*(t_s; t)$ is the stellar mass at time $t$ of a satellite accreted at time $t_s$, and $\tau_{\text{merg}}$ is the dynamical friction time scale of the satellite used to model the time it takes for the satellite to merge with the central after $t_s$. The function, $\mathcal{H}(x) = 1$ if $x > 0$ and $\mathcal{H}(x) = 0$ otherwise, is used to ensure that only satellites that can sink to the centre and merge with the primary contribute to the mass of the primary. The summation is over all satellites accreted into the host halo. In practice, the stellar mass of a galaxy is recorded in a number of time bins so that the addition of stellar mass owing to accretion is done separately for individual bins. Following Lu et al. (2014), we estimate the value of $R(\tau)$ from the spectral synthesis model of Bruzual & Charlot (2003) assuming a Chabrier IMF.

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### 4.3 In-situ star formation versus accretion

Figure 8 shows the fraction of stars formed in situ in present day central galaxies as a function of their host halo mass. The predictions of Model II are plotted as the green line (average) and the green shaded area (with the variance arising from different halo merger trees), while the predictions of Model III are plotted in red. The predictions of the two models are quite similar. For central galaxies in haloes with masses below $10^{12} h^{-1} M_\odot$, almost all the stars are formed in situ. This fraction decreases rapidly with
increasing halo mass at $M_h > 10^{12} h^{-1} M_\odot$. About 70\% of all stars in the central galaxy of a halo with $M_h \approx 10^{13} h^{-1} M_\odot$ are formed in situ; for cluster haloes with $M_h \sim 10^{15} h^{-1} M_\odot$, this fraction is about 15\%, so about 85\% of the stellar mass is acquired through accretion.

4.4 Downsizing versus upsizing

Galaxies of different masses have different star formation (assembly) histories. To characterise these histories in a more quantitative way, we examine the characteristic redshift, $z_f$, by which a fraction $f$ of the final stellar mass in a galaxy has formed (or assembled). Figure 7 shows the distribution of galaxies in the $z_{0.5}$ - $z_{0.1}$ plane for star formation (green contours) and stellar mass assembly (red contours), with the contours delineating the isodensity lines that contain 90\% of all the galaxies. The results are again shown for haloes with five different present-day masses, as indicated in the panels, predicted by Model II (the upper 5 panels) and Model III (the lower 5 panels), respectively. For the most massive haloes [$M_h(z = 0) > 10^{14} h^{-1} M_\odot$], the star formation time and the assembly time differ considerably, especially in $z_{0.5}$. On average about 50\% of the stellar mass in the central galaxies of such massive haloes form before $z = 4$, but assemble much later at $z \approx 1$. For haloes with masses lower than $10^{13} h^{-1} M_\odot$, the star formation time and assembly time are almost identical, indicating that central galaxies in such haloes acquire their stars mostly through in situ star formation, as we have already seen in the last subsection. A Milky Way mass galaxy [$M_h(z = 0) \sim 10^{12} h^{-1} M_\odot$] on average formed about 10\% of its stars by $z \approx 2$ and about 50\% after $z = 1$. For dwarf galaxies residing in haloes with $M_h(z = 0) < 10^{11} h^{-1} M_\odot$, Model III predicts diverse formation redshifts. For example, the majority of galaxies residing in $10^{11} h^{-1} M_\odot$ haloes are predicted to form 10\% of their stars by about $z = 4$, while a fraction is predicted to form their first 10\% at much later times: $z \approx 1$. The diversity becomes larger for smaller galaxies: for galaxies in $3 \times 10^{10} h^{-1} M_\odot$ haloes, some show star formation as early as that in the central galaxy clusters, while others formed most of their stars after $z \approx 1$. This diversity owes to the transition in star formation efficiency at $z \approx 2$ and the variance in the halo accretion histories. Haloes that formed early generally have experienced an early burst phase of star formation, while younger haloes that assembled most of their mass later than the transition redshift did not have such an early star burst.

In Figure 8 we show how the averages of $z_{0.1}$ and $z_{0.5}$ change with halo mass for both star formation (green lines) and stellar mass assembly (red lines). For haloes with $M_h(z = 0) > 10^{11} h^{-1} M_\odot$, both Model II and Model III predict that the centrals of massive haloes on average form a fixed fraction of their stars earlier, a trend usually referred to as “downsizing”. A similar downsizing trend is also seen in the stellar mass assembly for haloes with $10^{11} h^{-1} M_\odot < M_h(z = 0) < 10^{13} h^{-1} M_\odot$. However, this trend breaks down in two ways. First, for the most massive haloes [$M_h(z = 0) > 10^{13} h^{-1} M_\odot$], more massive centrals actually assemble their stars later. At late times, these galaxies tend to build up their mass hierarchically by accreting satellite galaxies, resembling the mass assembly history of the dark matter haloes themselves. Second, although the downsizing trend holds for dwarf galaxies in Model II, the trend predicted by Model III is completely the opposite for these galaxies: on average smaller galaxies tend to be older. This again owes to the boost of star formation in low-mass haloes at high $z$ in Model III.

4.5 The global star formation history and the reionisation of the Universe

The solid green and red lines in Figure 9 show the star formation rate density (SFRD) predicted by Model II and Model III, respectively. These results take into account star formation in haloes down to a mass of $2 \times 10^6 h^{-1} M_\odot$. As shown in Lu et al. (2014), the boost in the SFRD at $z > 3$ of Model III relative to Model II is dominated by star formation in low-mass galaxies hosted by haloes with masses $M_h < 10^{10.5} h^{-1} M_\odot$. These galaxies are missed in the current observational data used to derive the SFRD, and so the discrepancy between the prediction of Model III and the observational results at $z > 3$ (shown as error bars in the figure) probably owes to incompleteness in the data. Indeed, if we use the same lower limit of UV magnitude adopted in Bouwens et al. (2012), which...
is $M_{\text{UV,AB}} = -17.7$, to predict the SFRD, we get the results shown by the dashed lines, which brings the prediction of Model III into much better agreement with the data. The change in the prediction of Model II is small, because in this model galaxies below the limit do not make a significant contribution. This demonstrates clearly the importance in observing and modelling very faint galaxies to understand the SFRD at high $z$.

If one assumes that the Universe is kept ionised by the UV photons from young stars, a minimal SFRD required can be estimated using the equation given by Madau et al. (1999):

$$\frac{\text{SFRD}_{\text{min}}(z)}{M_\odot \text{yr}^{-1} \text{Mpc}^{-3}} \approx 3 \times 10^{-4} \left( \frac{C}{f_{\text{esc}}} \right) \left( \frac{1 + z}{6} \right)^3,$$

where $C$ is the clumpiness factor of the IGM and $f_{\text{esc}}$ is the average escape fraction of UV photons from star forming galaxies. The normalisation factor here is based on the assumption of a Chabrier IMF (Chabrier 2003). The clumpiness factor is expected to evolve with redshift and its value is still quite uncertain. Madau et al. (1999) adopted $C = 30$ at $z = 5$ based on the cosmological simulation of Gnedin & Ostriker (1997). More recently, Bolton & Haehnelt (2007) claimed that $C$ at $z = 7$ may be as small as 5. For comparison we show in Figure[10] the minimum SFRD as a function of $z$ assuming $C = 30$ (solid blue line) and $C = 5$ (dashed blue line), with $f_{\text{esc}} = 0.2$ in both cases. Since SFRD$_{\text{min}}$ is directly proportional to $C/f_{\text{esc}}$, the predictions with other values of $C$ and $f_{\text{esc}}$ can be obtained by shifting the curves vertically. As one can see, if the clumpiness factor is as high as 30 at $z < 5$, Model II may not be able to keep the Universe ionised at $z > 4$, while Model III is able to do so over the entire redshift range between $z = 0$ to $z = 6$. More quantitatively, to keep the Universe re-ionised at $z \leq 6$, Model III needs $C/f_{\text{esc}} \gtrsim 50$, while Model II needs $C/f_{\text{esc}} \lesssim 8$. Unfortunately, without better constraints on $C$ and $f_{\text{esc}}$, no stronger statement can be made about the two models.

5 MERGERS AND THE TRANSFORMATION OF GALAXIES

5.1 Last major merger

Figure[10] shows the redshift of the last major merger of present-day central galaxies as a function of host halo mass. The predictions of Model II and Model III are shown in green and red, respectively. Lines are the averages, while the shaded areas enclose the 95% range of variance owing to different merger histories.

The prediction that the brightest central galaxies (BCGs) in clusters on average have experienced a major merger in the recent past suggests that many of the present-day BCGs should have distorted morphologies and/or close companions signifying a recent major merger or one expected in the near future. By inspecting images of BCGs at low $z$, McIntosh et al. (2008) and Tran et al. (2013) found that a significant fraction of them indeed show signatures of recent major mergers. This fraction may be even higher at higher $z$ (Burke & Collins 2013). All these observations indicate that major mergers are quite frequent for BCGs, consistent with our model predictions.

5.2 Merger-driven morphology transformations

As a simple model, we assume that stellar disks form only through in situ star formation, and that a major merger can transform a stellar disk into a spheroid. The mass of the stellar disk is then simply the total mass of stars formed in situ after the last major merger. Based on this we use the ‘bulge-to-total’ ratio, $B/T$, to characterise the major merger-driven morphologies of present-day galaxies. It should be cautioned, however, that a galactic bulge can be formed in other ways, such as the secular evolution of the disk. The bulge fraction defined here, therefore, can only be taken as a lower limit and serves as a simple indicator of how much a central galaxy may be disturbed by infalling satellites.

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Figure 11 shows the distribution of $B/T$ for present-day central galaxies in four halo mass bins. In cluster haloes, owing to the frequent bombardment of massive satellites even at late times, central galaxies are almost completely bulges, i.e. ellipticals. For haloes in the mass range $10^{12} h^{-1} M_\odot$ to $10^{13} h^{-1} M_\odot$ in situ star formation begins to quench at the present time while major mergers are sparse but not negligible (see Figure 3). Consequently, central galaxies in such haloes experience either one or no major merger in the recent past, and the last major merger is probably the only major merger that has ever occurred after the host halo leaves the active star formation band as it grows. Thus, the central galaxy is either dominated by bulge, if it has experienced a recent major merger, or remains disk dominated, if such a merger did not occur. This explains the strong bimodality in their $B/T$ distribution.

In our model, galaxies with $B/T \approx 1$ would all be 'elliptical' galaxies. However, centrals in massive clusters and lower mass groups ($M_h \sim 10^{12} h^{-1} M_\odot$) have quite different assembly histories, which may leave different imprints in their dynamical and morphological properties. As shown in Figure 12 centrals in cluster haloes have on average experienced about 5 major mergers and an even larger number of minor mergers during the last period of low in situ star formation (defined, quite arbitrarily, as the period after the in situ star formation rate declines to 1/3 of the peak value), while most of the centrals in lower-mass groups have on average only experienced $\approx 1.5$ major mergers and no more than 3 mergers with a mass ratio $> 0.1$. The total amount of stellar mass acquisition through mergers with $r \geq 1/3$ is also significant, about 50% for centrals in massive halos, and about 25% for centrals of $10^{13} h^{-1} M_\odot$ halos, as shown by the dashed curves in Figure 12. Furthermore, as shown in Figure 3 the merger events of cluster central galaxies can be considered as 'dry' since their star formation has been quenched more than 10 Gyrs ago. In contrast, a large fraction of 'centrals' in lower-mass group haloes are still close to the regime of active star formation while experiencing mergers. Observations show that the properties of elliptical galaxies change systematically with luminosity: the most luminous ellipticals, such as the BCGs, tend to be boxy and show little rotation, while ellipticals of intermediate luminosity are more disky and tend to possess significant rotational support (e.g. Kormendy & Bender 1996 Kormendy et al. 1996). These differences most likely reflect the differences in the formation processes. For instance, Naab & Burkert (2003) showed that mergers between progenitors with mass ratios of the order of 1:3 produce remnants with morphologies and kinematics that are more similar to the intermediate-luminosity ellipticals than to those produced by mergers with equal masses. Cox et al. (2006) showed that the remnants of dissipational and dissipationless mergers are different, with the former exhibiting a variety of rotation signatures while the latter have little rotation. Our star formation and assembly histories can be combined with detailed modelling of the dynamics of mergers to understand the origin of massive elliptical galaxies. In particular, our results cast doubt on the scenario in which the late growth and structure of BCGs.
are assumed to be determined by minor mergers (e.g. Bezanson et al. 2009; van Dokkum et al. 2010; Hilz et al. 2013). Indeed, as shown in Figure 12, BCGs have on average experienced about 5 major mergers, with significant mass acquisition, in the late ‘dry’ merger phases, and major mergers must have played an important role in their evolution.

For a Milky Way sized galaxy with $M_\odot(0) = 10^{11.5} - 10^{12.5} h^{-1} M_\odot$, in situ star formation has dominated, while major mergers have been rare since $z \approx 2$. These galaxies, therefore, remain disk dominated, free of any significant major merger - driven bulge components.

The predictions of Model II and Model III differ when it comes to dwarf galaxies. For Model II, major mergers between dwarf galaxies are extremely rare. Most of them do not experience any major merger at all (Figure 10). Therefore, all the stars are expected to remain in a disk (see the upper panel of Figure 11). For Model III, however, most of the galaxies experienced some major mergers during their initial star burst phases (Figure 4). The exact time when a major merger occurs has large variations. Some galaxies may have their last major merger just before the end of the initial star burst at $z \approx 2$, while others had their last major mergers much earlier (Figure 10). Major mergers are very rare at $z < 2$ while in situ star formation continues, allowing the growth of new disks. The fraction of stars contained in the spheroid depends both on when the last major merger occurs and on the star formation efficiency that follows. This complexity in star formation history results in diverse morphologies of present day dwarfs, as shown in Figure 17.

Dwarf elliptical (dE) and dwarf Spheroidal (dSph) galaxies tend to reside in dense environments, and many of them tend to be supported by velocity dispersion rather than rotation (e.g. Geha et al. 2003; Toloba et al. 2013). Various theories have been proposed to explain their origin. One of the most popular scenarios is galaxy harassment (Moore et al. 1996), in which high speed encounters of a dwarf disk with other galaxies in a dense environment is assumed to heat up the disk and transform it into a dE or a dSph. However, the predicted kinematics, which shows significant rotation, is at odds with the the observational results. Our result here suggests that some of the slow rotators may be the remnants of early major mergers between dwarf galaxies. The lower panel of Figure 13 shows that dwarf satellites predicted by Model III are somewhat skewed towards higher $B/T$ than their counterparts in the field. This is not true in Model II, where all the dwarf galaxies are strongly disk dominated. However, the predicted fraction of bulge-dominated satellites is too low to account for the total population of dE’s and dSph’s. It is likely that later evolution, such as harassment, may transform the disk component, making the bulge components more dominant. Note that the difference between present day centrals and satellites is quite small because many of the satellites today were accreted quite late and because our prediction does not account for any morphological transformations after a galaxy becomes a satellite.

It should be pointed out that the above discussion is based on the value of $r$, namely the ratio between the original secondary mass and the primary mass. As shown above, our model predicts that only a fraction, $f_{TS} \approx 0.4$, of the original mass of the secondary is added to the central after a merger while the rest is stripped and deposited as halo stars. If the stripping occurred at large distances from the central, the secondary mass at the time of merger would be $r \times f_{TS}$. For comparison, the values of this quantity are labelled on the top of Figure 12. As is clear, in this case major mergers, still defined by a mass ratio $\geq 1/3$, would be rare for all galaxies. However, this scenario may not be realistic. Observations show that halo stars are mostly identified around central galaxies and, as we will see below, the amount of halo stars predicted by our models is consistent with observations (Bernardi et al. 2013). This suggests that stripping of stars most likely occurs when the secondary is close to the primary, and so the mass ratio, $r$, defined above is more relevant when considering the mutual gravitational interaction between the merging galaxies.

6 STELLAR POPULATIONS

6.1 Stellar ages

Observationally, the star formation histories (SFHs) of individual galaxies can be estimated from their stellar populations. One popular way to do this is to use the spectra of galaxies, which contain information about the SFH, initial mass function (IMF), chemical enrichment history and dust content of galaxies. In Figure 14, we compare the average stellar ages predicted by Model II and Model III with the observational results of SDSS galaxies obtained by Gallazzi et al.
The observational stellar ages are determined by simultaneously fitting five spectral absorption features that break some degeneracies in spectral synthesis parameters. The weighted age of a galaxy is defined as

$$\text{Age} = \frac{\int_0^\infty \text{SFR}(t) f(t) t \, dt}{\int_0^\infty \text{SFR}(t) f(t) \, dt},$$

where $f(t)$ is either the fraction of the remaining stellar mass or the luminosity of a simple stellar population with age $t$. In Figure 14 we plot the average ages weighted either by stellar mass (red bands) or by the r-band luminosity (green bands). The observational ages, with the median shown by the solid line and the 16 and 84 percentile by the dashed lines, are also weighted by the r-band luminosity, so a direct comparison between the model and the data can be made. The SDSS galaxies cover a stellar mass range between $10^9$ and $10^{12} M_\odot$, where the observed age increases with stellar mass generally, and increases sharply around $10^{10} M_\odot$. The model predictions agree with the observational data only qualitatively: the predicted ages are systematically older than that observed between $10^9 M_\odot$ and $10^{10} M_\odot$. Similar discrepancies have also been found by [Lu Y. et al. 2013] using semi-analytic models.

This discrepancy may indicate an intrinsic deficiency in the approach adopted here or in similar approaches in the literature. By matching only SMFs of galaxies, our model may be insensitive to the star formation history in the recent past. For example, an enhancement in recent star formation may contribute little to the total stellar mass, and so is not well captured in our model, but can significantly increase the optical luminosity, thereby decreasing the light-weighted age. As a demonstration, the upper cross in Figure 14 shows the stellar mass weighted age of stars in the LMC based on the star formation history derived from the colour magnitude diagram of resolved stars [Weisz et al. 2013]. Our model predictions match the observation well. For comparison, the lower cross shows the r-band luminosity-weighted age obtained from the same star formation history with our adopted spectral synthesis model. The age so obtained lies below the green band, because our average model underpredicts the current star formation rate of the LMC.

There are uncertainties in the observational data too. It is in general difficult to distinguish stars that formed about 8-10 Gyrs ago from those that formed 4-5 Gyrs ago from an analysis of the optical-NIR spectra (e.g. [Bruzual & Charlot 2003; Pacifici et al. 2012]. Basically the UV light provides information about recent star formation, while strong Balmer absorption lines are sensitive only to intermediate-age (1-3 Gyrs old) stars, but one cannot distinguish stars older than 4 Gyrs. Thus, it is possible that the average stellar ages derived from the observational data have missed the contribution of such an old population.

6.2 Halo Stars

In the simple prescription adopted here for galaxy mergers, a constant fraction $f_{TS}$ of the original stellar mass of the merging satellite is accreted by the central, and the rest is deposited in a diffuse component, referred to as intracluster stars in clusters or as halo stars in general. As shown in Tables 1 and 2, the value of $f_{TS}$ is constrained to be about 40%, although the uncertainty is quite large. This low value of $f_{TS}$ is driven predominantly by the observed SMFs at the massive end, i.e. with $M_\ast \gtrsim 10^{11} M_\odot$ corresponding to $M_h > 10^{13} h^{-1} M_\odot$. Had we set $f_{TS} = 1$, i.e. if all the original mass in an accreted satellite were added to the central, we would get a SMF that is shown by the thick black line in Figure 14. This SMF is significantly higher than the observational data of [Baldry et al. 2012] used to constrain our model (data

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Recent analyses show that the most massive galaxies (with $M_\ast > 10^{11} M_\odot$) tend to have extended wings in their light profiles. This makes the luminosity (stellar mass) measurements of these galaxies quite uncertain. As shown by Bernardi et al. (2013) and He et al. (2013), using different methods and light profiles to fit galaxy images can lead to a factor of 2 difference in the estimated luminosity of a massive galaxy. The effect on the derived SMF can be seen in Figure 15 from the difference between the red line compared to the green line. It is interesting to note that our model prediction assuming $f_{TS} = 1$ is consistent with the SMF obtained by Bernardi et al. (2013) using the magnitudes within the entire Sersic profiles (the red line) obtained by Simard et al. (2011). This suggests that the halo component defined in our model may simply be the extended profiles of massive galaxies that are missing in the SMFs we use to constrain models. This interpretation is important implications for how dry mergers may affect the structure of BCGs.

The stellar mass function of galaxies predicted by Model III (grey line) in comparison to the prediction of the same model but assuming no stripping of satellites, i.e. $f_{TS} = 1$ (the thick black line). The data points are the observational data of Baldry et al. (2012). The green line is the SMF obtained by Bernardi et al. (2013) using SDSS 'cmodel' magnitudes, while the red line is the result obtained by the same authors using the magnitudes within the entire Sersic profiles (i.e. integrated to infinity) obtained by Simard et al. (2011).

Figure 15. The stellar mass function of galaxies predicted by Model III (grey line) in comparison to the prediction of the same model but assuming no stripping of satellites, i.e. $f_{TS} = 1$ (the thick black line). The data points are the observational data of Baldry et al. (2012). This problem cannot be solved by simply adjusting other parameters in our empirical model characterised by equation (2). At $M_h \lesssim 10^{13} h^{-1} M_\odot$, the model parameters are well constrained by the SMFs at $M_\ast \lesssim 10^{11} M_\odot$, where galaxies are built mainly through in situ star formation. At $M_h \gtrsim 10^{13} h^{-1} M_\odot$, although the SFR is not well constrained at low $z$, it is negligible compared to the mass accretion from satellites. The build-up of cluster centrals at low $z$ is, therefore, mainly determined by the halo merger trees and the value of $f_{TS}$.

Recent analyses show that the most massive galaxies (with $M_h > 10^{13} M_\odot$) tend to have extended wings in their light profiles. This makes the luminosity (stellar mass) measurements of these galaxies quite uncertain. As shown by Bernardi et al. (2013) and He et al. (2013), using different methods and light profiles to fit galaxy images can lead to a factor of 2 difference in the estimated luminosity of a massive galaxy. The effect on the derived SMF can be seen in Figure 15 from the difference between the red line compared to the green line. It is interesting to note that our model prediction assuming $f_{TS} = 1$ is consistent with the SMF obtained by Bernardi et al. (2013) using the magnitudes within the entire Sersic profiles (the red line) obtained by Simard et al. (2011). This suggests that the halo component defined in our model may simply be the extended profiles of massive galaxies that are missing in the SMFs we use to constrain models. This interpretation is important implications for how dry mergers may affect the structure of BCGs.

Figure 16 shows the ratio between the total mass of halo stars and the stellar mass of the central galaxy as a function of host halo mass. Note that the following numbers are only valid if the stellar mass is measured as in Baldry et al. (2012). If one uses the method of Bernardi et al. (2013), the mass ratio is close to zero. In a cluster as massive as $10^{15} h^{-1} M_\odot$, the mass in the diffuse component is about 2 - 3 times as high as that of the central galaxy. In a group sized halo of mass $\sim 10^{13} h^{-1} M_\odot$, the total mass in halo stars is comparable to the mass of the central galaxy. The ratio then drops rapidly towards lower halo mass. In a Milky Way mass halo, the predicted ratio is only a few percent. However, the results for low-mass haloes should be taken with caution. As mentioned above, our model assumes a constant $f_{TS}$ and this parameter is constrained mainly by the SMFs at the massive end. It is unclear whether the same number also applies to galaxies with lower masses. The upturn predicted by Model III at the low-mass end again owes to the boosted star formation at high $z$ in low-mass haloes.

To understand the stellar population of the halo stars, we make a census of their formation time and location, in terms of redshift and the stellar mass of the host galaxy in which they formed, respectively. We show the result by the solid contours in Figure 17. For comparison, we also plot the results for stars in...
the central galaxies as the dashed contours. Because galaxy stellar mass and stellar metallicity are found to be correlated for local galaxies (Gallazzi et al. 2005), the mass of the host galaxy where a star forms may be used to indicate its metallicity. The stellar metallicity increases with stellar mass for galaxies with stellar masses below $2 \times 10^{10} M_\odot$ and becomes saturated at about solar metallicity above this mass (indicated by the horizontal lines in Figure 17).

Compared to the stars in the central galaxy, the halo stars in a Milky Way sized halo form a distinct population: they are systematically older and formed in lower-mass progenitors (hence poorer in metals). The mass weighted age of the halo stars is roughly 9 - 30 Gyr, while the average age of the stars in the central galaxy is about 6 Gyr, as shown in Figure 18. If we apply the same local stellar mass-metallicity relation (Gallazzi et al. 2005) to high-z galaxies, the average metallicity of the halo stars is about 3 times lower. Our results are qualitatively consistent with the recent observations of M31 (Bernard et al. 2014). For a massive cluster, the halo stars and those in the central galaxies occupy almost the same region in the $M_\star(z) - z$ plane (see the lower panel of Figure 17), although the halo stars appear to be slightly younger. Most of the stars are formed in galaxies with stellar masses $\gtrsim 10^{10} M_\odot$. Thus the stellar populations in both the central galaxy and the halo component are quite homogeneous, with ages of $\sim 10$ Gyr and with nearly solar metallicity. This prediction can be checked by studying the stellar age and metallicity of halo stars in clusters.

7 SUMMARY AND DISCUSSION

In a previous paper (Lu et al. 2014), we developed an empirical model to describe the star formation rates of central galaxies in haloes of different masses at different redshifts. A series of nested models were constructed to accommodate more and more observational constraints. We found that Model II, which represents a class of ‘Slow Evolution’ models in the literature, can reproduce the SMFs since $z = 4$, but fails to accommodate the cluster galaxy luminosity function, the steep SFR-functions at high $z$, and the old stellar population seen in local dwarf galaxies. We also found that Model III is the simplest model family that can match well all these observational data. In the present paper, we use the same models, but with model parameters updated with recent observational data of the galaxy SMFs at high $z$. The results presented here confirm and re-enforce those of Lu et al. (2014). In particular, the constrained Model III pre-

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**Figure 17.** The solid contours show the formation redshift and location (i.e. the stellar mass of the galaxy) of the halo stars. Red, green and blue contours enclose 30%, 60% and 90% of the stars, respectively. The dashed contours are the same as the solid ones but for stars in central galaxies. We only show Model III (Model II is similar). Results are shown for Milky Way mass haloes (upper panel) and massive cluster haloes (lower panel). The horizontal lines mark $M_\star = 2 \times 10^{10} M_\odot$, above which the stellar metallicity begin to saturate (Gallazzi et al. 2005).

**Figure 18.** The mass weighted ages of halo stars (HS, solid lines) and of stars in central galaxies (dashed lines) as a function of the host halo mass. The predictions of Model II and Model III are plotted in green and red, respectively.
dicts much steeper SMFs at $z \geq 4$ than Model II, and that a significant amount of star formation may be hosted by low-mass haloes at high $z$ to keep the Universe ionised. Since the publication of Lu et al. [2013], two additional studies have presented evidence in support of this picture [Madau et al. 2014, Weisz et al. 2014]. These results suggest that the class of ‘Slow Evolution’ models in the literature [Yang et al. 2013; 2014]. These results suggest that the class of ‘Slow Evolution’ models in the literature [Yang et al. 2013; 2014], in which star formation in haloes with $M_\star$ suppression at high $z$, are insufficient to describe the evolution of the galaxy population.

We use our constrained model parameters to make predictions for a number of properties of the star formation and stellar mass assembly histories. The results are summarised in the following.

First, the evolution of the galaxy population is found to be characterised by a number of characteristic halo mass scales:

(i) A mass scale of $10^{13} h^{-1} M_\odot$ at $z = 0$, decreasing to $\sim 3 \times 10^{12} h^{-1} M_\odot$ at $z > 2$, above which in situ star formation drops rapidly, and the central galaxies experience frequent major mergers most of which will be dry.

(ii) A mass scale of $3 \times 10^{11} h^{-1} M_\odot$ at $z = 0$, increasing to $10^{12} h^{-1} M_\odot$ at high $z$, at which the efficiency of in situ star formation reaches a maximum, with a SFR as high as about half of the baryon accretion rate into the host halo. Major mergers are rare in this halo mass range.

(iii) A mass scale of $10^{11} h^{-1} M_\odot$ at $z > 3$, below which in situ star formation has a rate about 0.1 times the baryon accretion rate into the host halo. On average, one or two major mergers are expected to occur for the central galaxies.

Second, galaxies hosted by haloes of different masses follow distinct star formation and assembly histories. Based on the characteristic halo mass scales given above, central galaxies can be divided roughly into three different categories according to their formation and assembly histories:

(i) For haloes with $M_h > 10^{13} h^{-1} M_\odot$, a strong in situ star formation rate declines rapidly after reaching its peak value, and is followed by significant accretion of stars from satellites. For such massive systems, more massive haloes tend to assemble their stellar mass later, contrary to the downsizing trends observed for lower mass galaxies.

(ii) For haloes with masses $10^{11} h^{-1} M_\odot < M_h < 10^{13} h^{-1} M_\odot$, mass assembly by accretion of satellites is not important, and the star formation is delayed relative to the formation of the host halo.

(iii) For haloes with masses below $10^{11} h^{-1} M_\odot$, assembly by accretion is again unimportant. The star formation history is characterised by a burst at $z > 2$ and a nearly constant star formation rate after $z = 1$. The relative importance of the early star formation increases with decreasing halo mass, and the ‘downsizing’ trend is reversed.

Third, we use the merger history of the model galaxies to predict the bulge to total mass ratios of present galaxies. The average bulge mass fraction is found to depend strongly on halo mass:

(i) In cluster sized haloes with $M_h > 3 \times 10^{13} h^{-1} M_\odot$, almost all the centrals are ellipticals formed through frequent major mergers.

(ii) In group sized haloes with masses between $3 \times 10^{12} h^{-1} M_\odot$ and $3 \times 10^{13} h^{-1} M_\odot$, the distribution of the bulge-to-total ratio of the central galaxies is strongly bimodal. Those galaxies that experienced a recent major merger are spheroid dominated, whereas the others are free of any significant merger-driven bulge.

(iii) For haloes with masses $3 \times 10^{11} h^{-1} M_\odot < M_h < 3 \times 10^{12} h^{-1} M_\odot$, central galaxies with a significant merger-driven bulge are extremely rare.

(iv) For dwarf galaxies, half of them have significant (with $B/T > 10\%$) spheroidal components formed during their early star burst phase ($z > z_c \approx 2$). Satellite galaxies of similar masses tend to have a larger bulge fraction than centrals.

We emphasise again that bulges can form in various other ways than through major mergers, and that our prediction only applies to major merger-driven bulges.

Finally, we have made predictions for the amount of halo stars, and when and where these stars form in comparison with stars in the corresponding central galaxies. The results are:

(i) In a Milky Way mass halo, the total mass in halo stars is 2 to 5 percent of the mass of the central galaxy, and this number increases to $\sim 100\%$ in haloes with $M_h \sim 10^{13} h^{-1} M_\odot$, and to about 200% to 300% in massive clusters.

(ii) In a Milky Way mass halo, the stars in the central galaxy and halo stars form two distinct stellar populations, with the latter being older and poorer in metals by a factor of $\sim 3$. In contrast, these two components form a quite homogeneous population (old and with solar metallicity) in massive clusters.

All these results are obtained in an empirical way, independent of any detailed assumptions about the underlying physical processes that drive the evolution of the galaxy population. Clearly, our results should be compared with the predictions of numerical simulations and/or semi-analytical models to constrain theories of galaxy formation. We will come back to this in a forthcoming paper.

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