Nuclear superfluidity for antimagnetic rotation in $^{105}\text{Cd}$ and $^{106}\text{Cd}$

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Abstract

The effects of nuclear superfluidity on antimagnetic rotation bands in $^{105}\text{Cd}$ and $^{106}\text{Cd}$ are investigated by the cranked shell model with the pairing correlations and the blocking effects treated by a particle-number conserving method. The experimental moments of inertia and the reduced $B(E2)$ transition values are excellently reproduced. The nuclear superfluidity is essential to reproduce the experimental moments of inertia. The two-shears-like mechanism for the antimagnetic rotation is investigated by examining the shears angle, i.e., the closing of the two proton hole angular momenta, and its sensitive dependence on the nuclear superfluidity is revealed.

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I. INTRODUCTION

Most rotational bands are usually observed in nuclei with substantial quadrupole deformations. In these bands, the states decay by strong electric quadrupole ($E2$) transitions and the energy spectra show a pronounced rotational character. Such bands are usually interpreted as the result of a coherent collective rotation of many nucleons around an axis perpendicular to the symmetry axis.

In the 1990’s, however, a new type of rotational band with strongly enhanced magnetic dipole ($M1$) transitions and very weak $E2$ transitions has been discovered experimentally in nearly spherical light Pb isotopes [1]. This new type of rotational bands have been discovered experimentally in a number of nearly spherical nuclei in $A = 80, 110, 135, \text{ and } 190$ mass regions [1–4]. The interpretation of such bands in terms of the shears mechanism was firstly given in Ref. [5]. In order to distinguish this kind of rotation from the usual rotation in well-deformed nuclei, the term “magnetic rotation” (MR) was introduced [5].

In analogy to the antiferromagnetism in condensed matter physics, a similar phenomenon known as “antimagnetic rotation” (AMR) is predicted in nuclei by Frauendorf [3, 7]. The AMR band can be explained by the two-shears-like mechanism: in some specific nearly spherical nuclei, two valence protons (neutrons) are aligned back to back in opposite directions, nearly perpendicular to the orientation of the total spin of the neutrons. A rotational band can be built on such a near-spherical nucleus since the rotational symmetry is violated by the nucleon currents. Higher angular momenta is obtained by simultaneously aligning the two angular momenta for the valence protons (neutrons) toward the neutron (proton) angular momentum vector.

AMR is expected to be observed in the same mass regions as MR [3]. However, it differs from MR in two aspects. First, there is no $M1$ transition in the AMR band since the transverse magnetic moments of the magnetic subsystems are antialigned. The resulting transverse magnetic moment is zero. Second, as the antimagnetic rotor is symmetric with respect to a rotation by $\pi$ about the total angular momentum axis, the AMR bands consist of regular sequences of energy levels differing in spin by $2\hbar$ and are connected by weak $E2$ transitions reflecting the nearly spherical core. Moreover, the phenomenon of AMR is characterized by a decrease of the $B(E2)$ values with spin. Since AMR was proposed [3], it has been investigated both from experimental and theoretical aspects. To date, experimental
evidence of AMR has been reported in Cd isotopes including $^{105}$Cd, $^{106}$Cd, $^{108}$Cd, $^{110}$Cd, $^{112}$Cd. Most recently, two AMR bands in a single nucleus are firstly observed in $^{107}$Cd. In addition, the occurrence of this phenomenon still needs further investigation by lifetime measurements in $^{109}$Cd, $^{100}$Pd, $^{144}$Dy, $^{101}$Pd, and $^{112}$In.

Theoretically, AMR has been discussed by simple geometry in the classical particle rotor model, and the tilted axis cranking (TAC) model. Based on the TAC model, many applications have been carried out in the framework of microscopic-macroscopic model, and pairing plus quadrupole model. Most recently, the TAC model based on the covariant density functional theory is used to investigate the AMR with the point coupling effective interaction PC-PK1, for its review see Ref. 4. The quality of the cranking approximation for principal-axis cranking, tilted-axis cranking, and aplanar tilted-axis cranking has been discussed and tested within the particle rotor model.

In the present work, the cranked shell model (CSM) with the pairing correlations treated by a particle-number conserving (PNC) method is used to investigate the AMR bands in $^{105,106}$Cd. The PNC-CSM method is proposed to treat properly the pairing correlations and the blocking effects, and it has been applied successfully for describing the odd-even differences in moments of inertia (MOI’s), the nonadditivity in MOI’s, the microscopic mechanism of identical bands, the non-existence of nuclear pairing phase transition, etc. The high-spin states and high-$K$ isomers in the rare-earth, the actinide region and superheavy nuclei are also well described in the PNC-CSM scheme. In contrary to the conventional Bardeen-Cooper-Schrieffer (BCS) or Hartree-Fock-Bogolyubov (HFB) approach, the Hamiltonian is solved directly in a truncated Fock-space in the PNC method. Therefore, the particle-number is conserved and the Pauli blocking effects are taken into account exactly. The PNC scheme has been used both in relativistic and non-relativistic mean field models in which the single-particle levels are calculated from the self-consistent mean-field potentials instead of the Nilsson potential.
II. THEORETICAL FRAMEWORK

The cranked shell model Hamiltonian of an axially symmetric nucleus in the rotating frame can be written as

\[
H_{CSM} = H_0 + H_P = H_{Nil} - \omega J_x + H_P ,
\]  

(1)

where \(H_{Nil}\) is the Nilsson Hamiltonian, \(-\omega J_x\) is the Coriolis interaction with the cranking frequency \(\omega\) about the \(x\) axis (perpendicular to the nuclear symmetry \(z\) axis). \(H_P\) is the pairing interaction,

\[
H_P = -G \sum_{\xi \eta} a_\xi^\dagger a_\eta^\dagger a_\xi a_\eta ,
\]  

(2)

where \(\bar{\xi}(\bar{\eta})\) labels the time-reversed state of a Nilsson state \(\xi(\eta)\), \(G\) is the effective strength of monopole pairing interaction.

Instead of the usual single-particle level truncation in conventional shell-model calculations, a cranked many-particle configuration (CMPC) truncation (Fock space truncation) is adopted \([30, 46]\). By diagonalizing the \(H_{CSM}\) in a sufficiently large CMPC space, sufficiently accurate solutions for low-lying excited eigenstates of \(H_{CSM}\) can be obtained. An eigenstate of \(H_{CSM}\) can be written as

\[
|\Psi\rangle = \sum_i C_i |i\rangle , \quad (C_i \text{ real}),
\]  

(3)

where \(|i\rangle\) is a CMPC (an eigenstate of the one-body operator \(H_0\)). The expectation value of a one-body operator \(O = \sum_{k=1}^N O(k)\) is thus written as

\[
\langle \Psi | O | \Psi \rangle = \sum_i C_i^2 \langle i | O | i \rangle + 2 \sum_{i<j} C_i C_j \langle i | O | j \rangle .
\]  

(4)

As \(O\) is a one-body operator, the matrix element \(\langle i | O | j \rangle\) for \(i \neq j\) is nonzero only when \(|i\rangle\) and \(|j\rangle\) differ by one particle occupation \([30]\). After a certain permutation of creation operators, \(|i\rangle\) and \(|j\rangle\) can be recast into

\[
|i\rangle = (-1)^{M_{\mu}'} |\mu \cdots \rangle , \quad |j\rangle = (-1)^{M_{\nu}'} |\nu \cdots \rangle ,
\]  

(5)

where the ellipsis “\(\cdots\)” stands for the same particle occupation and \((-1)^{M_{\mu(\nu)'}} = \pm 1\) according to whether the permutation is even or odd. Therefore, the expectation value of \(O\)
can be separated into the diagonal and the off-diagonal parts

$$O = \langle \Psi | O | \Psi \rangle = \left( \sum_\mu O(\mu) + 2 \sum_{\mu<\nu} O(\mu\nu) \right), \quad (6)$$

$$O(\mu) = \langle \mu | O | \mu \rangle n_\mu, \quad (7)$$

$$O(\mu\nu) = \langle \mu | O | \nu \rangle \sum_{i<j} (-1)^{M_i\mu+M_j\nu} C_i C_j, \quad (8)$$

where $n_\mu = \sum_i |C_i|^2 P_{i\mu}$ is the occupation probability of the cranked Nilsson orbital $|\mu\rangle$ and $P_{i\mu} = 1 \ (0)$ if $|\mu\rangle$ is occupied (empty) in $|i\rangle$.

The kinematic moment of inertia $J^{(1)}$ of $|\Psi\rangle$ can be written as

$$J^{(1)} = \frac{1}{\omega} \langle \Psi | J_x | \Psi \rangle. \quad (9)$$

The $B(E2)$ transition probabilities can be derived in the semiclassical approximation as

$$B(E2) = \frac{3}{8} \langle \Psi | Q_{20}^p | \Psi \rangle^2, \quad (10)$$

where $Q_{20}^p$ correspond to the quadrupole moments of protons and

$$Q_{20} = \sqrt{\frac{5}{16\pi}} (3z^2 - r^2) = r^2 Y_{20}. \quad (11)$$

III. RESULTS AND DISCUSSIONS

The Nilsson parameters ($\kappa$ and $\mu$) of $^{105,106}$Cd are taken from the Lund systematics [47]. The quadrupole deformation parameters are taken as $\varepsilon_2 = 0.12$ and $\varepsilon_2 = 0.14$ for $^{105}$Cd and $^{106}$Cd, respectively. These values are close to those used in the TAC calculations based on the microscopic-macroscopic model or the covariant density functional theory [9, 22]. The valence single-particle space in this work is constructed in the major shells from $N = 0$ to $N = 5$ both for protons and neutrons, so there is no effective charge involved in the calculation of the $B(E2)$ values. The effective pairing strengths can, in principle, be determined by the odd-even differences in nuclear masses and the MOI’s, and are connected with the dimension of the truncated CMPC space. The dimensions of the CMPC space are about 1000 both for protons and neutrons. The corresponding effective pairing strengths used in this work are $G_p = 0.45$ MeV and $G_n = 0.80$ MeV for $^{105}$Cd, $G_p = 0.45$ MeV and $G_n = 0.45$ MeV for $^{106}$Cd. The data show that the MOI’s for the AMR band in $^{105}$Cd are smaller than those in $^{106}$Cd. Therefore, a larger effective neutron pairing strength for $^{105}$Cd
is adopted. A larger CMPC space with renormalized pairing strengths gives essentially the same results. In addition, the stability of the PNC-CSM calculation results against the change of the dimension of the CMPC space has been investigated in Refs. 30, 34, 41. In the present calculations, almost all the important CMPC’s (with the corresponding weights larger than 0.1%) are taken into account, so the solutions to the low-lying excited states are accurate enough.

![Cranked Nilsson Levels](image)

**FIG. 1.** (Color online). The cranked Nilsson levels near the Fermi surface of $^{106}$Cd for (a) protons and (b) neutrons. The positive (negative) parity levels are denoted by blue (red) lines. The signature $\alpha = +1/2$ ($\alpha = -1/2$) levels are denoted by solid (dotted) lines. The deformation parameter $\varepsilon_2 = 0.14$.

The cranked Nilsson levels near the Fermi surface of $^{106}$Cd for (a) protons and (b) neutrons are given in Fig. [1]. The positive (negative) parity levels are denoted by blue (red) lines. The signature $\alpha = +1/2$ ($\alpha = -1/2$) levels are denoted by solid (dotted) lines. Because the Nilsson levels of $^{105}$Cd are very similar with those of the $^{106}$Cd, we do not show them here. It can be seen from Fig. [1] that the two proton holes for $^{105,106}$Cd are $\pi 9/2^+ [404] (\pi g_9/2)$. The data show that the AMR bands in $^{105}$Cd [8] and $^{106}$Cd [9] are the lowest lying negative and positive parity band, respectively. The lowest lying negative parity band for $^{105}$Cd in our
calculation is $\nu 1/2^- [550](h_{11/2})$ and the lowest lying positive parity band for $^{106}$Cd is the yrast band. Therefore, in the following investigation, we do nonadiabatic calculations for the $\nu 1/2^- [550]$ band in $^{105}$Cd and the yrast band in $^{106}$Cd.

![Figure 2](image_url)

**FIG. 2.** (Color online). The experimental (solid circles) and calculated kinematic MOI's $J^{(1)}$ with (solid black lines) and without (dashed red lines) pairing correlations for (a) $^{105}$Cd and (b) $^{106}$Cd.

Figure 2 shows the experimental (solid circles) and calculated kinematic MOI's $J^{(1)}$ with (solid black lines) and without (dashed red lines) pairing correlations for $^{105}$Cd (upper panel) and $^{106}$Cd (lower panel). The pairing interaction is very important in reproducing the experimental MOI’s, especially the upbending. It can be seen that the MOI’s of $^{105,106}$Cd are overestimated when the pairing interaction is switched off, while they are well reproduced after considering the pairing correlations. The first backbending in $^{105}$Cd at $\hbar \omega \approx 0.4$ MeV is caused by aligning one neutron pair $\nu g_{7/2}$. The configuration after backbending in $^{105}$Cd is thus $\nu h_{11/2}(g_{7/2})^2$ coupled to a pair of $\pi g_{9/2}$ proton holes, which is consistent with the
previous calculations \cite{8,22}. The first backbending in $^{106}$Cd at $\hbar \omega \approx 0.3$ MeV is caused by one pair of neutrons jumping from $\nu g_{7/2}$ to $\nu h_{11/2}$.

FIG. 3. (Color online). The experimental (solid circles) and calculated $B(E2)$ values with (solid black lines) and without (dashed red lines) pairing correlations for (a) $^{105}$Cd and (b) $^{106}$Cd. The blue dotted line in (b) is the calculated results with a reduced deformation of $\varepsilon_2 = 0.12$ in which the pairing is considered. The data for $^{105,106}$Cd are taken from \cite{8,9}.

One of the typical features of AMR is the weak $E2$ transitions reflecting the small deformation of the core. Moreover, the corresponding $B(E2)$ values rapidly decrease with the angular momentum, which is connected with the interpretation of the two-shears-like mechanism. Figure 3 shows the experimental (solid circles) and calculated $B(E2)$ values with (solid black lines) and without (dashed red lines) pairing correlations for $^{105}$Cd (upper panel) and $^{106}$Cd (lower panel). It can be seen that the decreasing tendency of the $B(E2)$
values with the cranking frequency can be obtained no matter the pairing correlation is considered or not. However, the agreement between the data and the calculated results is further improved by taking the pairing correlation into account, especially for the higher rotational frequency region. For $^{105}$Cd, with paring correlations, the expectation value of $Q_{20}$ decreases from 0.55 eb to 0.41 eb with the rotational frequency $\hbar \omega$ increasing from 0.45 MeV to 0.75 MeV. The $Q_{20}$ value and the corresponding $B(E2)$ value are reduced to about 75\% and 55\%, respectively, which are caused by the effect of the cranking. For $^{106}$Cd, it is difficult to describe the $B(E2)$ behavior with a frozen deformation parameter. This may be due to the deformation change with the rotational frequency for $^{106}$Cd. In fact, as show in the blue dotted line in Fig. 3(b), in order to reproduce the $B(E2)$ behavior from $\hbar \omega = 0.45$ MeV to $\hbar \omega = 0.75$ MeV, a corresponding deformation change from $\varepsilon_2 = 0.14$ to $\varepsilon_2 = 0.12$ is necessary. Therefore, it can be seen that the two-shears-like mechanism alone can provide the decrease of the $B(E2)$ values in $^{105}$Cd, while additional reduction of the deformation is needed for $^{106}$Cd. 

![Angular momentum vectors of neutrons $J_\nu$ and the two $\pi g_{9/2}$ proton holes $j_\pi$, (a) without pairing (b) with pairing, at rotational frequencies from 0.5 to 0.7 MeV in $^{105}$Cd.](image)

**FIG. 4.** (Color online). Angular momentum vectors of neutrons $J_\nu$ and the two $\pi g_{9/2}$ proton holes $j_\pi$, (a) without pairing (b) with pairing, at rotational frequencies from 0.5 to 0.7 MeV in $^{105}$Cd.

In order to examine the two-shears-like mechanism for the AMR band, we show the
angular momentum vectors of neutrons $J_\nu$ and the two $\pi g_{9/2}$ proton holes $j_\pi$ at rotational frequencies from 0.5 to 0.7 MeV in $^{105}$Cd in Fig. 4. It should be mentioned that, in the principal axis cranking model, the expectation value of $J_z$ vanishes due to the conservation of signature. In the present AMR bands, the two proton holes in both $^{105}$Cd and $^{106}$Cd are paired. This means that the total angular momentum projection $K$ of these two proton holes should always be zero. The angular momenta of the two proton holes could, in principle, be extracted exactly from the TAC calculation. Here, we calculate $J_z$ approximately in the following way according to Ref. [27]

$$J_z = \sqrt{\langle \Psi|J_z^2|\Psi \rangle}.$$  

(12)

This method has been proved to be a good approximation by comparing the principal axis cranking with the particle rotor model in Ref. [27]. It can be seen from Fig. 4 that the two proton angular momentum vectors $j_\pi$ are pointing opposite to each other and are nearly perpendicular to the vector $J_\nu$ at $\hbar \omega = 0.5$ MeV. The abrupt increasing of neutron angular momentum alignment from $\hbar \omega = 0.5$ to 0.6 MeV in Fig. 4(a) is due to level crossing. After considering the nuclear superfluidity, the level crossing is delayed and the neutron angular momentum alignment increases gradually, which is consistent with the data. With increasing cranking frequency the gradual alignment of the vectors $j_\pi$ of the two $\pi g_{9/2}$ proton holes toward the vector $J_\nu$ generates angular momentum while the direction of the total angular momentum stays unchanged. This leads to the closing of the two shears. The two-shears-like mechanism can thus be clearly seen. It should be noted that the closing of the two proton hole angular momenta becomes more obvious when the pairing correlation is taken into account. This indicates the important role played by the the nuclear superfluidity in AMR.

IV. SUMMARY

In summary, antimagnetic rotation bands in $^{105}$Cd and $^{106}$Cd are investigated by the cranked shell model with the pairing correlations treated by a particle-number conserving method and the blocking effects taken into account exactly. The experimental moments of inertia in $^{105}$Cd and $^{106}$Cd are excellently reproduced with the proper treatment of the nuclear superfluidity. The reduced $B(E2)$ transition depends on the deformation rather than the
superfluidity. The calculated $B(E2)$ values in $^{105}$Cd are in good agreement with the data. In order to reproduce the $B(E2)$ values in $^{106}$Cd, a corresponding deformation change is necessary. The two-shears-like mechanism for the antimagnetic rotation is investigated and its sensitive dependence on the nuclear superfluidity is revealed.

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