The Gaia–WISE Extragalactic Astrometric Catalog

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Abstract

The Gaia mission has detected a large number of active galactic nuclei (AGNs) and galaxies, but these objects must be identified among the thousandfold more numerous stars. Extant astrometric AGN catalogs do not have the uniform sky coverage required to detect and characterize the all-sky, low-multipole proper motion signals produced by the barycenter motion, gravitational waves, and cosmological effects. To remedy this, we present an all-sky sample of 567,721 AGNs in Gaia Data Release 1, selected using WISE two-color criteria. The catalog has fairly uniform sky coverage beyond the Galactic plane, with a mean density of 12.8 AGNs per square degree. The objects have magnitudes ranging from $G = 8.8$ down to Gaia’s magnitude limit, $G = 20.7$. The catalog is approximately 50% complete but suffers from low stellar contamination, roughly 0.2%. We predict that the end-of-mission Gaia proper motions for this catalog will enable detection of the secular aberration drift to high significance (23σ) and will place an upper limit on the anisotropy of the Hubble expansion of about 2%.

Key words: astrometry – catalogs – galaxies: active – infrared: galaxies – proper motions – quasars: general

Supporting material: machine-readable table

1. Introduction

The Gaia mission will provide astrometric and proper motion measurements for a large number of bright active galactic nuclei (AGNs), but separating the $\sim 10^6$ extragalactic objects from the $\sim 10^9$ stars remains challenging (Gaia Collaboration et al. 2016). Current catalogs include the Large Quasar Astrometric Catalog (LQAC; Souchay et al. 2015), the Véron Catalog of quasars and AGNs (Véron-Cetty & Véron 2010), the Secrest et al. (2015) catalog of mid-infrared AGNs, and the Gaia Universe Model Snapshot (GUMS), a simulated catalog (Robin et al. 2012). Many of these catalogs are dominated by the Sloan Digital Sky Survey (SDSS) footprint that covers 35% of the sky (Ahn et al. 2012), which is problematic for all-sky proper motion studies that attempt to detect low-multipole correlated proper motion signals such as the secular aberration drift dipole (Xu et al. 2012; Titov & Lambert 2013; Truebenbach & Darling 2017b), the stochastic gravitational wave background quadrupole (Gwinn et al. 1997; Book & Flanagan 2011; Titov et al. 2011; Darling et al. 2018), or the isotropy of the Hubble expansion (Darling 2014; Chang & Lin 2015; Bengaly 2016).

Desirable features of extragalactic proper motion catalogs are all-sky, uniform selection, and low stellar contamination. Completeness is not very important: it impacts the signal-to-noise of correlated global proper motions, which scales with the square root of the number of objects. In this work, we consider only low-multipole proper motion signals, but completeness will ultimately determine the maximum multipole that can be studied due to the limiting sky density of sources. Stellar contamination is the largest concern for detecting global signals of a few $\mu$arcsec year$^{-1}$ because stellar proper motions can be large and significant and therefore dominate the individually insignificant extragalactic proper motions. What stellar contamination remains in any given extragalactic catalog may be addressed using a non-Gaussian permissive likelihood function as described in Darling et al. (2018).

This paper presents the Gaia–WISE extragalactic astrometric catalog, a catalog designed to have low stellar contamination and fairly uniform sky coverage outside of the Galactic Plane. Section 2 presents the WISE color–color selection used to identify AGNs and exclude stars, and Section 3 explores the sky distribution of the catalog, its optical and mid-IR properties, its redshift distribution, and the expected end-of-mission proper motion uncertainties. Section 4 predicts the performance of this catalog in detecting the secular aberration drift caused by the barycenter acceleration about the Galactic Center. Section 4 also predicts the expected Gaia sensitivity to anisotropy in the Hubble expansion. We discuss the ramifications of this work and the future prospects for extragalactic proper motion studies in Sections 5 and 6. We assume a Hubble constant of $H_0 = 72 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and a flat cosmology (other cosmological assumptions are not required).

2. Catalog Selection Method

The WISE survey is an all-sky mid-infrared (MIR) survey in the 3.4, 4.6, 12, and 22 $\mu$m bandpasses ($W1$, $W2$, $W3$, and $W4$, respectively; Wright et al. 2010). The AllWISE data release, used in this work, combines data from the cryogenic and post-cryogenic (Mainzer et al. 2011) survey phases, and provides better sensitivity and accuracy over previous WISE data releases. WISE colors have been shown to cleanly separate AGNs from stars and normal galaxies, and several methods exist in the literature for selecting AGNs with WISE (e.g., Stern et al. 2005, 2012; Mateos et al. 2012; Assef et al. 2013; Truebenbach & Darling 2017a). To create our catalog of Gaia AGNs, we did not consider selection methods using only a $W1–W2$ color cut in order to avoid contamination from brown dwarfs at low Galactic latitudes, which can reside in the color space selected by single-color cuts (Kirkpatrick et al. 2011).

We employed the ALLWISE catalog of MIR AGNs described in Secrest et al. (2015). The catalog is based on the WISE two-color selection technique of Mateos et al. (2012), which has cuts in the $W1–W2$ and $W2–W3$ color space, referred
to as the color wedge. This AGN color wedge was defined based on the Bright Ultrahard XMM-Newton survey (BUXS), one of the largest flux-limited samples of “ultrahard” X-ray-selected AGNs, but the method does not employ X-ray selection directly. BUXS is comprised of 258 objects, of which 56.2% are type 1 AGNs and nearly the rest are type 2. BUXS type 2 AGNs are intrinsically less luminous than type 1 AGNs. Since the completeness of the MIR wedge has a strong dependence on luminosity, the wedge preferentially selects type 1 AGNs. Secrest et al. (2015) selected 1.4 million MIR AGNs using ALLWISE profile-fitting magnitudes with S/N ≥ 5 and the color wedge criteria of Mateos et al. (2012). They included an additional constraint of limiting their selections to ALLWISE sources with \texttt{co\_flags} = “0000” to avoid sources contaminated by image artifacts.

We cross-matched the Secrest et al. (2015) catalog of MIR AGNs with \textit{Gaia} Data Release 1 using \texttt{allwise\_best\_neighbour}, the precomputed \textit{WISE} cross-match table provided in the \textit{Gaia} archive (Marrese et al. 2017). The table includes only the most likely matches between the \textit{WISE} and \textit{Gaia} catalogs, called “best neighbours.” Since \textit{Gaia} is used as the leading catalog in cross-matching, a \textit{Gaia} source may be matched to multiple sources from an external catalog. Marrese et al. (2017) then determined the best match to the \textit{Gaia} source using the angular distance, position errors, epoch difference, and density of sources in the external catalog. A small number of \textit{Gaia} sources have \(G > 21\), fainter than \textit{Gaia}’s nominal magnitude limit of 20.7, which are likely incorrectly determined magnitudes (Gaia Collaboration et al. 2016). Such objects were excluded from the cross-match. Additionally, all stars from the Tycho 2 survey were removed to avoid stellar contamination, which excluded 65 objects. We discuss possible further stellar contamination in Section 2.2. The resulting catalog of \textit{Gaia} MIR AGNs contains 567,721 objects. The first 10 objects are given in the Appendix, and the full catalog is available online.

2.1. Completeness

The completeness of the \textit{WISE} color wedge selection is dependent on the ratio of the AGN luminosity to the host luminosity because host galaxy light can contaminate the MIR emission (Mateos et al. 2012; Padovani et al. 2017). Thus, lower luminosity AGNs will have the colors of normal galaxies and will be excluded by the color wedge. To assess the completeness of our catalog, we compared the catalog to the sample of SDSS DR9 QSOs (Ahn et al. 2012) in \textit{Gaia}. SDSS QSOs were identified in the \textit{Gaia} source catalog via the cross-matching algorithm provided in the \textit{Gaia} archive with a matching radius of 1 arcsecond. Of these \textit{Gaia}-SDSS QSOs, 44.6% were also identified by the \textit{WISE} color wedge, suggesting that our sample is missing more than half of all AGNs in the \textit{Gaia} catalog. Only 49.3% of \textit{Gaia}-SDSS QSOs have S/N > 5 detections and zero contamination and confusion flags in all three \textit{WISE} bands; most of the incompleteness of the \textit{Gaia–WISE} catalog is therefore due to non-detections in the least-sensitive \textit{WISE} \textit{W3} band. Among the \textit{WISE}-detected \textit{Gaia}-SDSS QSOs, 90.2% lie in the \textit{WISE} MIR color wedge. The remaining quasars generally have bluer \textit{W1–W2} colors than the color wedge, likely due to contamination by host galaxy starlight.

2.2. Stellar Contamination

Mateos et al. (2012) found that contamination by normal galaxies in the MIR wedge is minimal. For astrometric purposes, however, objects need only be extragalactic, so unresolved galaxies are acceptable. Contamination by Galactic stars is of much greater concern due to their large proper motions.

To assess any remaining stellar contamination after omitting the Tycho stars, we cross-matched our sample with the SDSS DR12 catalog (Alam et al. 2015). In our sample, 229,073 AGNs reside within the SDSS footprint, and 65,575 have a spectroscopic classification from SDSS. Of those, only 104 objects (0.16%) are identified by their spectroscopic classification as stars. Extrapolating to the whole sky gives approximately 910 total stars in our sample, suggesting negligible contamination from stars. We also consider contamination from dusty stars that would not be found in our SDSS cross-match. Nikutta et al. (2014) find that a majority of objects brighter than \(W1 = 11\) are Galactic stars. Our sample contains 1836 objects with \(W1 < 11\), which indicates a maximum of 0.32% contamination from dusty stars.

3. Results

3.1. Sky Distribution

\textit{Gaia} surveys the sky down to \(G = 20.7\), with a small fraction of objects at \(G > 21\) (Gaia Collaboration et al. 2016). As illustrated in Figure 2, the majority of \textit{WISE} AGNs lie at the fainter end of \textit{Gaia}’s magnitude distribution. Statistics for the distribution of \textit{G} magnitudes are listed in Table 1.

3.2. Optical Properties

\textit{Gaia} surveys the sky down to \(G = 20.7\), with a small fraction of objects at \(G > 21\) (Gaia Collaboration et al. 2016). As illustrated in Figure 2, the majority of \textit{WISE} AGNs lie at the fainter end of \textit{Gaia}’s magnitude distribution. Statistics for the distribution of \textit{G} magnitudes are listed in Table 1.

3.3. Mid-IR Properties

The \textit{WISE} two-color distribution for our catalog is shown in Figure 3, along with the Mateos et al. (2012) wedge. The majority of objects reside in a locus near the bluer end of the color wedge, with a small number of outliers with redder colors. The distribution around the locus tapers before the color cuts, suggesting that the color wedge captures most of the AGN population, except for the bottom right cut where AGN colors begin to overlap with the color space occupied by normal galaxies. The distributions of \textit{WISE} \textit{W1}, \textit{W2}, and \textit{W3} magnitudes, and \(W1–W2\) and \(W2–W3\) colors are shown in Figure 4; statistics for these distributions are given in Table 1.
3.4. Redshifts

Redshifts were obtained for objects with spectroscopic redshifts from SDSS. Redshifts with nonzero warning flags or negative errors were discarded, since a negative redshift error indicates a poor fit even if the warning flag is zero. This yielded redshifts for 90,365 objects (∼15%). The redshift distribution is shown in Figure 5. Note that this distribution is incomplete and subject to selection bias due to targeted quasar surveys by SDSS and thus the corresponding redshift sensitivity biases. The catalog contains 202 redshifts above $z = 4$, which is unexpectedly high considering Gaia’s magnitude limit. However, a majority of these are confirmed quasars in the SDSS Baryon Oscillation Spectroscopic Survey quasar catalog, of which many were selected for the survey using WISE colors (Pâris et al. 2017).

3.5. Proper Motion Uncertainties

Gaia DR2 will include positions, proper motions, and parallaxes—or limits on these quantities—for all objects. Predicted proper motion standard errors can be calculated ahead of the release using Gaia performance characteristics. The PyGaia Python toolkit is an implementation of Gaia performance models that can be used for basic simulation and analysis of Gaia data, including calculation of proper motion uncertainties. We utilized the PyGaia Python toolkit to calculate predicted proper motion uncertainties for each AGN, shown in Figure 6. This calculation relies on each object’s $G$ magnitude, $V-I_C$ color, and ecliptic latitude. For objects where the $V-I_C$ color was not available, this value was set to zero, which has a negligible impact on the predicted proper motion uncertainty. The reported uncertainties include known instrumental effects. Statistics for the distributions of predicted uncertainties are given in Table 1. The uncertainties in R.A. proper motion are generally larger than those in decl., which is a consequence of Gaia’s scanning law.

4. Applications

Although proper motions for Gaia AGNs will not be available until DR2, we can use the predicted uncertainties to test Gaia’s potential capability to detect or constrain select proper motion signals. For this purpose, we generate a null proper motion catalog by randomly selecting proper motions consistent with zero based on each object’s expected errors and assuming Gaussian-distributed errors. One can then add proper motion signals to the noisy null catalog to study the expected sensitivity of the Gaia–WISE catalog to various correlated proper motions. These include the secular aberration drift (Section 4.1), an anisotropic Hubble expansion (Section 4.2), and a stochastic long-period gravitational wave background (Darling et al. 2018).

1. http://www.cosmos.esa.int/web/gaia/science-performance
Table 1

|       | G (mag) | W1 (mag) | W2 (mag) | W3 (mag) | W1–W2 (mag) | W2–W3 (mag) | Redshift | \(\sigma_{\alpha, R.A.}^{\mu} \) (\(\mu\)as yr\(^{-1}\)) | \(\sigma_{\beta, \text{Decl.}}^{\mu} \) (\(\mu\)as yr\(^{-1}\)) |
|-------|---------|----------|----------|----------|-------------|-------------|----------|---------------------------------|---------------------------------|
| Mean  | 19.3    | 15.2     | 14.0     | 10.9     | 1.2         | 3.0         | 1.3      | 236                             | 218                             |
| Median| 19.4    | 15.3     | 14.1     | 11.1     | 1.2         | 3.0         | 1.2      | 205                             | 191                             |
| Minimum| 8.8     | 4.8      | 3.7      | 0.2      | 0.5         | 2.0         | 0.0      | 2                               | 3                               |
| Maximum| 21.0    | 18.8     | 17.1     | 12.9     | 2.2         | 5.8         | 7.0      | 1062                            | 797                             |

Note.

\(^{a}\) Gaia expected end-of-mission proper motion uncertainty (see Section 3.5).

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![Figure 3](image-url)

**Figure 3.** **WISE** colors for Gaia MIR AGNs. The dashed lines indicate the color wedge of Mateos et al. (2012). The color bar indicates the logarithm of the number of objects per hexagonal bin.

### 4.1. Secular Aberration Drift

The aberration of light is an apparent angular deflection of light rays caused by an observer’s velocity across the rays and the finite speed of light. Aberration can be caused by the Earth’s annual motion or the secular solar motion in the Galaxy or with respect to the cosmic microwave background rest-frame. If the observer experiences a constant acceleration then the aberration will exhibit a secular drift that manifests as an apparent proper motion of objects in a dipole pattern converging toward the acceleration vector direction.

The secular aberration drift caused by the solar system’s acceleration toward the Galactic Center (a consequence of its orbit) is detectable in extragalactic proper motions as a dipole vector field that resembles an electric field and converges on the Galactic Center (e.g., Xu et al. 2012; Titov & Lambert 2013; Truebenbach & Darling 2017b). The expected solar acceleration and corresponding secular aberration drift dipole amplitude can be predicted using the distance to the Galactic center (\(R_0\)) and the orbital speed of the Sun (\(\Theta_0 + V_0\)), which includes solar motion \(V_0\) in the direction of Galactic rotation \(\Theta_0\): \(a = (\Theta_0 + V_0)^2/R_0\) and \(|\mu| = a/c\). Reid et al. (2014) measured \(R_0 = 8.34 \pm 0.16\) kpc and \(\Theta_0 + V_0 = 255.2 \pm 5.1\) km s\(^{-1}\) from the trigonometric parallaxes and proper motions of masers associated with young massive stars. These yield an acceleration of \(a = 0.80 \pm 0.04\) cm s\(^{-1}\) yr\(^{-1}\) and a dipole amplitude of \(|\mu| = 5.5 \pm 0.2\) \(\mu\)as yr\(^{-1}\).

An E-mode vector field dipole painted on the sky, \(V_E(\alpha, \delta)\), can be expressed as a \(\ell = 1\) vector spherical harmonic following the notation of Mignard & Klioner (2012):

\[
V_E(\alpha, \delta) = \left( s_{11}^{\Re} \frac{1}{2} \sqrt{\frac{3}{\pi}} \sin \alpha + s_{11}^{\Im} \frac{1}{2} \sqrt{\frac{3}{\pi}} \cos \alpha \right) \hat{e}_n \\
+ \left( s_{10}^{\Re} \frac{1}{2} \sqrt{\frac{3}{2\pi}} \cos \delta + s_{11}^{\Re} \frac{1}{2} \sqrt{\frac{3}{\pi}} \cos \alpha \sin \delta \\
- s_{11}^{\Im} \frac{1}{2} \sqrt{\frac{3}{2\pi}} \sin \alpha \sin \delta \right) \hat{e}_b,
\]

where the coefficients \(s_{\ell m}^{\Re,\Im}\) determine the direction and amplitude of the dipole, \(\alpha\) and \(\delta\) are the R.A. and decl. coordinates, and \(\hat{e}_n\) and \(\hat{e}_b\) are the unit vectors in those directions. In this formalism, the expected E-mode dipole caused by the solar orbit about the Galactic Center (266\(^\circ\), \(-29\)^\(\circ\)) is \((s_{10}^{\Re}, s_{11}^{\Re}, s_{11}^{\Im}) = (-7.71 \pm 0.34, 0.615 \pm 0.027, -9.82 \pm 0.44) \mu\)as yr\(^{-1}\).

In order to predict the Gaia sensitivity to the secular aberration drift signal, we assigned a proper motion to each object that is consistent with no proper motion by randomly sampling its predicted Gaussian proper motion error distribution (Section 3.5). Over 1000 random trials, we added the expected secular aberration drift signal to the noisy null proper motions, omitting the uncertainties in the input dipole, and used a least-squares minimization to fit a dipole to the data. The resulting mean of the best-fit parameters is \((s_{10}^{\Re}, s_{11}^{\Re}, s_{11}^{\Im}) = (-7.73 \pm 0.48, 0.606 \pm 0.337, -9.79 \pm 0.36) \mu\)as yr\(^{-1}\), consistent with the original input dipole, with a mean Z-score of 23. We therefore predict that Gaia will produce the best determination of the secular aberration drift to date.

### 4.2. Anisotropic Cosmic Expansion

Extragalactic proper motions can test the isotropy of the Hubble expansion in the current epoch. If we neglect the peculiar motions of galaxies caused by density inhomogeneities, an isotropic Hubble expansion produces no extragalactic proper motions. In contrast, anisotropic expansion will cause extragalactic objects to stream toward directions of faster...
expansion and away from directions with slower expansion. All-sky proper motion observations can therefore measure the expansion isotropy and constrain cosmological models that attempt to explain accelerating expansion without invoking dark energy, such as Lemaitre–Tolman–Bondi models and Bianchi universes (e.g., Amendola et al. 2013).

**Figure 4.** Distribution of $W_1$, $W_2$, and $W_3$ band magnitudes, and $W_1$–$W_2$ and $W_2$–$W_3$ colors in the Gaia–WISE extragalactic astrometric catalog. The green dotted lines show the nominal S/N = 5 magnitudes for each band (16.9, 16.0, and 11.5 for $W_1$, $W_2$, and $W_3$, respectively).

**Figure 5.** Distribution of redshifts in the Gaia–WISE extragalactic astrometric catalog, where available (Section 3.4).

**Figure 6.** Predicted proper motion uncertainties in both R.A. (blue) and decl. (pink), with overlapping values shown in magenta.
The principal shearing axes can be arbitrarily oriented on the sky, and Darling (2014) showed that the proper motion induced by this anisotropy model can be completely described by a quadrupolar E-mode vector field.

To test the catalog’s potential to constrain anisotropy, we performed 1000 trials of adding a randomly generated anisotropy signal to the noisy null proper motions and fitting the anisotropy model to attempt to recreate the original input signal. We used the shear equation (Equation A1) of Darling (2014) to form these artificial anisotropy signals. For each trial, shear terms \( \Sigma_x, \Sigma_y, \) and \( \Sigma_z \) were drawn from Gaussian distributions with a mean of zero and a random standard deviations sampled from a uniform distribution between 0 and 0.1. The rotation angles were randomly selected from a uniform distribution between 0 and \( 2\pi \), assuming that there is no preferred direction for anisotropy. After the signal is added to the null proper motions, we use a least-squares minimization to fit the shear equation to the data in an attempt to recover the original signal.

The shear equation parameters are degenerate due to the rotation degeneracy of the principal axes (no particular axis is required to be the direction of maximum or minimum expansion), and therefore individual fit parameters do not necessarily match the original input parameters. Instead, we compare the maximum input shear to the maximum fit shear, as shown in Figure 7. There is a roughly one-to-one correlation for large input values; however, for maximum input shear below \( \sim 3 \times 10^{-2} \), noise dominates and the fit parameters tend toward a noise floor of 0.018 (a 1.8% departure from isotropy). The fit, however, is not significant for such low input anisotropy. For larger inputs where the fits are significant, we recover the input anisotropy with an uncertainty of about \( \pm 0.01 \).

### 5. Discussion

Prior to the first Gaia data release, the GUMS simulated a synthetic catalog of objects that Gaia could have potentially observed (Robin et al. 2012). GUMS simulated that nearly one million quasars would be observed by Gaia. Our sample roughly agrees with that number, given that it is about 50% incomplete. However, unlike GUMS, our sample consists of real objects actually detected by Gaia.

The Large Quasar Astrometric Catalog (LQAC3; Souchay et al. 2015), is a collection of 321,957 objects and represents the complete set of already identified quasars as of 2015. While the LQAC3 reliably contains extragalactic objects, the LQAC3-Gaia cross-match is dominated by the SDSS footprint. Our catalog has a more uniform sky distribution, and is therefore preferable for the study of low-multipole proper motion signals.

We expect Gaia–WISE AGNs to be able to measure the secular aberration drift with \( 2\sigma \) significance. Mignard (2012) predicted that Gaia would detect the secular aberration drift with about \( 10\sigma \) accuracy, assuming \( 10^3-10^5 \) quasars observed by Gaia with proper motion errors lower than predicted here. Titov et al. (2011) predicted Gaia to measure the dipole parameters with about \( 10\% \) relative precision. We find that the catalog should be able to measure the dipole parameters with higher precision, with the exception of the \( s_{11}^c \) component.

While isotropy is a fundamental pillar of cosmology and is well-constrained by the cosmic microwave background (Planck Collaboration et al. 2016), Gaia–WISE AGNs will be able to probe the isotropy of expansion for the relatively local universe since the majority are at redshift below 2.5 (95th percentile value). We predict that Gaia–WISE AGNs will place an upper limit on the anisotropy of the Hubble expansion of about 2\%. If the anisotropy is larger than about 3\%, then a significant measurement may be possible. Darling (2014) showed that the expansion is isotropic to within 7\% in the most constrained direction using a catalog of 429 radio sources. Local anisotropy has been previously measured using the Hubble parameters derived from SNe Ia. Chang & Lin (2015) found that the maximum anisotropy of the Hubble parameter is 3\% \( \pm 1\% \) for a set of supernovae in the redshift range \( z < 1.4 \). Bengaly (2016) find that the maximum variance of the Hubble parameter is \( (2.30 \pm 0.86) \) km s\(^{-1}\) Mpc\(^{-1}\) for \( z < 0.1 \), which corresponds to a maximum departure from isotropy of 3.3\% \( \pm 1.2\% \). The Gaia isotropy measurement will therefore
be competitive with and orthogonal to other more traditional methods.

Our analysis of the astrometric signals that may be detected using \textit{Gaia}–\textit{WISE} AGNs has assumed that the proper motions of all objects will be determined with the same precision as point sources. In reality, some galaxies may appear extended to \textit{Gaia}, in which case the precision of the image centroid position will be diminished. The intrinsic variability of AGNs will be an additional proper motion noise source, since variable AGN flux can cause the image centroid to move by up to a few mas for nearby AGNs (Popović et al. 2012). Microlensing of quasars may also cause the image centroid to shift due to the appearance or disappearance of microimages (Williams & Saha 1995; Lewis & Ibata 1998). The effect on the centroid position may be as large as tens of $\mu$as due to stellar mass objects in the lensing galaxy (Treyer & Wambsganss 2004) or a few mas due to stellar clusters (Popović & Simić 2013). The effects of both AGN variability and microlensing will add uncorrelated noise to the proper motions. They will therefore be averaged out in the determination of correlated signals such as the secular aberration drift and anisotropic expansion, despite adding to the overall noise in the signals.

\section{6. Conclusions}

We presented a catalog of \textit{Gaia} AGNs selected using the \textit{WISE} two-color method of Mateos et al. (2012). The catalog contains 567,721 objects, and we estimate that this sample is roughly 50\% complete. We find that the \textit{WISE} wedge reliably selects extragalactic objects, with only a negligible portion (0.2\%) of our sample likely contaminated by stars. We demonstrated two potential applications of the catalog, a precise measurement of the secular aberration drift and strong constraints on the isotropy of the Hubble expansion. Based on the expected end-of-mission proper motion uncertainty for each object in the \textit{Gaia}–\textit{WISE} catalog, we predict a measurement of the secular aberration drift with $\sim$23$\sigma$ significance and an upper limit on the anisotropy of the Hubble flow of $\sim$2\%.

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\textit{Software}: astropy (Astropy Collaboration et al. 2013), pyGaia, STILTS (Taylor 2006), TOPCAT (Taylor 2005).

\section{Appendix}

\textbf{Catalog}

Table 2 lists the first 10 rows of the \textit{Gaia}–\textit{WISE} extragalactic catalog. The full catalog containing 567,721 objects is available as a machine-readable table online and at http://vizier.u-strasbg.fr/vizier/.
Table 2
Gaia–WISE Extragalactic Catalog

| Gaia ID  | R.A. J2000 (°) | σR.A. (mas) | Decl. J2000 (°) | σDecl. (mas) | G (mag) | ALLWISE ID | W1 (mag) | σW1 (mag) | W2 (mag) | σW2 (mag) | W3 (mag) | σW3 (mag) | Redshift | Proper Motion Uncertainties* |
|----------|----------------|-------------|----------------|--------------|---------|------------|----------|-----------|---------|----------|---------|----------|----------|-------------------------|
| 4990063153917291776 | 0.00026196 | 0.4 | -47.64309208 | 0.4 | 18.637 | J000000.06-473835.1 | 14.086 | 0.027 | 13.233 | 0.028 | 9.987 | 0.048 | 81 | 81 |
| 2875546163053982464 | 0.00062956 | 2.6 | 35.51784342 | 1.0 | 18.537 | J000000.15+353104.1 | 14.522 | 0.030 | 13.372 | 0.031 | 10.663 | 0.102 | 108 | 108 |
| 234183672493897216 | 0.00066058 | 0.3 | -20.07434442 | 0.3 | 17.910 | J000000.15-200427.7 | 13.548 | 0.026 | 12.539 | 0.025 | 9.727 | 0.053 | 85 | 85 |
| 463568437412067840 | 0.00102928 | 1.2 | -78.53449449 | 1.4 | 20.226 | J000000.23-783204.1 | 15.212 | 0.031 | 13.694 | 0.028 | 10.388 | 0.055 | 336 | 336 |
| 230585125551067776 | 0.00142474 | 3.9 | -41.49299774 | 0.6 | 18.597 | J000000.33-412934.9 | 10.083 | 0.033 | 13.881 | 0.035 | 10.396 | 0.060 | 93 | 93 |
| 2747188660230483712 | 0.00191760 | 0.4 | 9.38565564 | 0.2 | 18.234 | J000000.46+092308.2 | 15.316 | 0.042 | 14.019 | 0.044 | 10.518 | 0.108 | 113 | 113 |
| 2420718373173082368 | 0.00308067 | 1.2 | -13.95693841 | 1.0 | 19.833 | J000000.73-135724.8 | 15.894 | 0.055 | 14.556 | 0.058 | 11.170 | 0.147 | 371 | 371 |
| 2341416058663072000 | 0.00345683 | 0.4 | -21.29793756 | 0.4 | 18.551 | J000000.82-211752.5 | 14.668 | 0.031 | 13.405 | 0.032 | 10.934 | 0.130 | 132 | 132 |
| 274494385199380480 | 0.00408179 | 1.3 | 4.82979136 | 0.4 | 19.661 | J000000.98-044971.7 | 15.503 | 0.044 | 13.987 | 0.044 | 10.764 | 0.112 | 1.62 | 1.62 |
| 274914737592463872 | 0.00424303 | 1.8 | 8.07294561 | 0.7 | 20.003 | J000001.02+080422.6 | 15.332 | 0.042 | 14.160 | 0.045 | 11.118 | 0.171 | 441 | 441 |

Note.
* Gaia expected end-of-mission proper motion uncertainty (see Section 3.5).
(This table is available in its entirety in machine-readable form.)
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