Optimising performance of a confocal fluorescence microscope with a differential pinhole

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Abstract

The signal-to-noise ratio (SNR)-resolution trade-off is of great importance to bio-imaging applications where the aim is to image the sample using as little light as possible without significantly sacrificing image quality. In this paper the inherent SNR-resolution trade-off in Confocal Fluorescence Microscopy (CFM) systems is presented by means of an effective tradeoff curve. A CFM system that employs a differential pinhole detection scheme has recently been shown to offer increased resolution, but at the expense of SNR. An optimum profile for the differential pinhole is identified in this paper that offers improved performance over a conventional (circular pinhole) system. The performance enhancement is illustrated through computer simulation.

Keywords: confocal fluorescence microscopy, resolution improvement, differential pinhole, image detection

(Some figures may appear in colour only in the online journal)
into the illumination structure by saturating the excited state of the fluorophores yielding a resolution in the 50-60 nm range [14]. A far-field technique, stimulated emission depletion microscopy (STED) has been demonstrated to yield an axial resolution of ~30nm [8]. Amongst the near-field techniques is near-field scanning optical microscopy (NSOM) which is capable of offering lateral resolution of ~20nm [8] when studying samples in close proximity (<10nm). NSOM achieves this by measuring near-field evanescent waves [15] using a probe close to the sample surface, discounting thereby the need for focusing using lenses. Single molecule localization based methods such as photo-activated localization microscopy (PALM) and stochastic optical reconstruction microscopy (STORM) have been shown to offer resolutions of ~20–30 nm in the lateral direction and ~50 nm in the axial direction [16]. However PALM and STORM require long exposure times and this limits their use in live-cell imaging. The principal drawback of all these techniques is the cost and complexity of their implementation as well as the extensive computational reconstruction that is often required.

When evaluating the performance of a microscope both the signal-to-noise ratio (SNR) and resolution need to be taken into consideration. The impact of one on the other is very apparent in confocal fluorescence microscopy (CFM) in which the SNR-resolution tradeoff is of great significance as fluorophores are vulnerable to photobleaching [17] and toxic cell damage [18]. In comparison to widefield fluorescence microscopy (WFM), CFM is more expensive and complex, but is widely used owing to its optical sectioning capability. CFM achieves this through its use of a detection pinhole, which by rejecting light away from the focal plane, makes optical sectioning possible. The lateral resolution in CFM improves by a factor ~√2 over WFM.

A small confocal pinhole, by limiting the number of photons reaching the detector, reduces the SNR but improves resolution by narrowing the mainlobe and reducing sidelobes of the CFM point spread function (PSF). For a CFM system with a given set of illumination and detection pupils the shape of the lateral point spread function is significantly influenced by the pinhole geometry (see equation (1)). By adjusting the pinhole to permit only the central peak viz., the infocus light, lateral resolution improvement is realised. Thus, the pinhole size, as well as its geometry, plays an important role in determining the resolving power and also the SNR of the system.

In this paper we investigate the use of an alternative pinhole geometry in CFM. This involves detecting two signals one from a central circular pinhole and the other from an annular region around the central region; this we designate as a ‘differential’ pinhole. The idea of using a differential pinhole has been discussed by various authors [19–22]. In references [19–21], physical pinholes are suggested, whereas in reference [22] the same concept is suggested but using a CCD detector array to emulate the pinholes. Segawa, Kozawa and Sato [23] discuss subtractive techniques for more general dual PSF microscopes, but the implementation of these is more complex requiring special polarised illumination.

The aim of this paper is to investigate the effect of varying the parameters describing a differential pinhole on resolution and SNR. Optimum parameters are identified and it is shown that the signal resulting from this design provides a significantly improved SNR-resolution trade-off than the circular pinhole used in existing CFM systems.

The organisation of the paper is as follows. The physical setup and key analytical expressions for SNR and resolution calculation are detailed in section 2. The impact of the differential pinhole on system performance is investigated in section 3. Section 4 presents computer-simulation results obtained using an optimum pinhole geometry.

2. CFM imaging and the SNR-Resolution trade-off

Consider an object illuminated by a lens (point spread function PSF) of a CFM system being imaged onto a detection plane using a detection lens (point spread function PSF). A detector is placed just after a pinhole in this plane with transmittance Pin(ν). For this system the 3D point spread function PSF is given by,

$$PSF(v, u) = PSF(v, u)(PSF(v, u)^*Pin(ν))$$ (1)

Here v and u are optical radial and optical axial coordinates related to object radial displacement r and object defocus z by equations (2) and (3) [24].

$$v = k r \sin \alpha$$ (2)

$$u = k z \sin^2 \alpha$$ (3)

where α is the lens semi-aperture angle, λ is the illumination wavelength and k = 2π/λ. For a lens with pupil P the 3D lens PSF intensity in polar coordinates for a small α is given by [25, 26].

$$PSF_{lens}(v, u) = \left[ 2\pi \int_0^1 \rho \exp\left( -\frac{j λ u^2}{2} \right) |J_0(νρ)|^2 ρ d\rho \right]$$ (4)

Here sin α ≈ αiπ which is the numerical aperture of either lens where a is the pupil radius, f is the focal length (assumed equal for both lenses under unity magnification). This is a good approximation if f ≫ a ≫ λ and a^2/f |f| ≪ 1 [25]. The final image is given by the convolution of the object fluorescence intensity with the system PSF [27]. We make the assumption throughout that the excitation and emission wavelengths are equal. For a particular 3D object with fluorophore concentration O(v, u), the image I(v, u) is then given by the 3D convolution (*),

$$I(v, u) = O(v, u)^*PSF(v, u)$$ (5)

The lateral resolution may be determined by computing the full-width half maximum (FWHM) of the PSF along the lateral direction. The axial resolution is computed by measuring the FWHM of the response of the system to a planar object as the axial resolution is computed by measuring the FWHM of the response of the system to a planar object as it is moved in the axial direction.

Amongst the various noise sources that degrade the signal quality in a CFM, shot noise has been acknowledged to be dominant in bio-imaging [28]. It is well known that the photon distribution is Poissonian. Thus, the mean and variance of the distribution are equal and the SNR can be readily calculated.
as the ratio of the mean number of detected photons (determined at the image plane) to standard deviation. We determine a normalised version of the SNR for a planar uniform object of unity fluorescence in the focal plane and for this case it reduces to the expression in equation (6), which has a maximum value of unity for a large detector pinhole.

\[
\text{SNR} = \sqrt{\frac{\text{mean detected photons}}{\text{mean detected photons}}} = \sqrt{\int 2\pi \text{ PSF}(\nu, u = 0) d\nu}
\]  

(6)

Figure 1 shows plots of SNR versus resolution in both axial and lateral directions calculated for a conventional circular pinhole. The curves characterise the SNR-resolution trade-off as the pinhole radius is varied.

Pinhole size and geometry play an important role in deciding the performance of a CFM system. Applications demanding a high SNR would require a large pinhole and this would invariably impede resolution. As can be seen from equation (1) the pinhole function directly affects the shape of the 3D PSF and experimenting with other pinhole shapes might offer a better SNR-resolution trade-off. In the next section we introduce the concept of a differential pinhole—an alternative pinhole arrangement that brings this about.

3. A Differential Pinhole

Consider an elliptical shaped pinhole (figure 2(b)) tilted an angle of 45 degrees as seen in figure 2(a) whose projection in the plane perpendicular to the optical axis (see figure 2(c)) assumes a circular shape defined mathematically by equation (7).

\[
\text{Pin}(r) = \begin{cases} 
1 & \text{for } r < r_i \\
-\gamma & \text{for } r_i < r < r_p \\
0 & \text{elsewhere}
\end{cases}
\]  

(7)

where \( r_p \) is the pinhole radius, \( r_i \) is the radius of the inner transparent annuli and \( \gamma \) is the multiplication factor applied to the photon counts from the second detector. Note that a similar output would be achieved by using a reduced reflectivity for the outer annulus but this would give an inferior SNR in the subtracted signal.

This detector arrangement could be implemented practically as shown in figure 2(a) by allowing different parts of the light onto separate detectors. Notably this arrangement requires two detectors (i.e. increased system cost) and the 45 degree tilt of the design would cause the different sides of the pinhole to be in slightly different planes. An alternative approach to overcome the above problems would be to employ a detector array and to sum appropriate pixels in a similar way to the arrangement in [22]. This detector array approach has the advantage that many different pinhole sizes and regions used for image formation may be selected from a single measurement. The advantage of the detector approach shown in figure 2(a) is that fast and high dynamic range detectors such as PMT’s may be used. For confocal applications, such as fluorescence lifetime imaging microscopy (FLIM) or fluorescence (cross-) correlation spectroscopy (FCS/FCCS), that demand very high speed data acquisition, point detectors such as PMTs prove more suitable than CCDs [29]. Expanding on the ideas laid down by Bertero [30] and Sheppard [31], ZEISS recently introduced the LSM 880 microscope that employs the so called Airyscan detector [32]; 32 individual detector elements functioning as pinholes capture all available light from an Airy disk simultaneously. At the expense of a slightly increased implementation cost (from the use of a reflective pinhole and two point detectors), the detector arrangement in figure 2, can offer similar data acquisition speeds to a conventional CFM.

If \( N_i \) and \( N \) denote the number of photons collected by detectors D1 and D2 respectively then the received signal \( S \) is given by \( N_i - \gamma N \) and the total noise variance by the sum

Figure 1. SNR-Resolution trade-off in the (a) lateral and (b) axial directions for a conventional circular pinhole as the pinhole radius is varied. The arrows indicate the direction of increasing pinhole radius; NA = 0.5 and \( \lambda = 0.5 \mu \text{m} \)
of the noise variances generated by D1 and D2 (see equation (8)). Thus the SNR of a CFM system using a differential pinhole is given by equation (9).

$$\sigma_{\text{diff}}^2 = N_+ + \gamma^2 N_-$$

$$\text{SNR}_{\text{diff}} = \frac{\Delta N_{\text{diff}}}{\sqrt{\sigma_{\text{diff}}^2}} = \frac{N_+ - \gamma N_-}{\sqrt{N_+ + \gamma^2 N_-}}$$

Three parameters can be used to define the shape of the differential pinhole projection defined in equation (7): $\alpha$, the ratio of the outer to the inner pinhole radius; $\gamma$, the multiplication factor applied to the photon count from the outer annulus; and $r_i$, the inner pinhole radius. This paper is concerned with the optimum choice of these parameters to give a good resolution whilst maintaining a good SNR. It is useful to see how variations in these parameters affect the point-spread functions. Figures 3(a) and (c) show the effect of changing $\alpha$ on the lateral confocal point-spread function. It may be seen that as $\alpha$ is increased the PSF mainlobe width reduces but at the expense of negative sidelobes. A similar pattern of PSF changes is observed in figure 3(c) when the multiplication factor is increased. However, clearly, this measure does not take into account the presence of the increasing negative sidelobes visible in figures 3(a) and (c). In order to take account of the negative effect of such sidelobes on imaging performance, we shall use an alternative measure of resolution designated as equivalent radius (ER). For lateral resolution the ER is defined as the radius of a circular top-hat function with a height of the maximum of the PSF and with the same volume as the modulus of the PSF. For the axial resolution ER is defined as the radius of a top-hat function with the height of the maximum of the axial response and with the same area as the modulus of the axial response. Mathematically, ER in the lateral direction $E_{\text{lat}}$ and axial direction $E_{\text{ax}}$ can be calculated as, in equations (10) and (11) respectively,

$$E_{\text{lat}} = \sqrt{\int |\text{PSF}(v)|dv}$$

$$E_{\text{ax}} = \int |\text{PSF}(u)|du$$

and importantly, these measures take into account the presence of side lobes in the PSFs. These ER measures are plotted as the bolder lines in figures 3(b) and (d) and it may be seen that as $\alpha$ and $\gamma$ increase the ER resolutions initially improve as the main lobe narrows but then deteriorate as the effect of the negative sidelobes increases.

As the pinhole geometry is controlled by three parameters and the result of changing any of these parameters will,
influence both the resolution and the SNR of the system; it is a complex task to try to find optimum conditions. To constrain the problem, we have imposed a constraint of always varying $r_i$ to generate a chosen SNR value. This value we have set at 0.5; this means that the differential pinhole with selected $\alpha$ and $\gamma$ values is assumed to be adjusted in overall radius so as to deliver a SNR of 0.5 (i.e. the same SNR as for a conventional confocal pinhole that admits 25% of the image-plane light). Constrained in this way, the resolution achievable for any $\alpha$ and $\gamma$ values can be found. These are plotted (as contour diagrams) for the lateral and axial (ER) resolutions in figures 4(a) and (b).

It may be seen, that in both the lateral and axial cases, a minimum is present in these plots, indicating that an optimum pairing of $\alpha$ and $\gamma$ exists. It is convenient that the optimum positions in both plots are closely aligned at around the $\alpha = 1.41$ and $\gamma = 1$ positions. Similar plots for different SNR values (below about 0.63) also show minima in these positions. This suggests that these values can be regarded as optimum in designing a differential pinhole. It is also interesting to examine the performance of a differential pinhole with these parameters by plotting, the type of resolution versus SNR characteristic plot shown in figure 2 and to compare with the plot for a conventional confocal pinhole. Figure 5 shows examples of these plots for the lateral and axial cases plotted both for the FWHM and the ER resolution criteria.

The bold dashed line in figure 5(b) marks the SNR threshold of 0.63 beyond which the differential pinhole based CFM system underperforms (worse SNR-resolution trade-off) with respect to a conventional (circular pinhole based) CFM system in the lateral direction. Below this threshold, the differential pinhole based CFM system offers maximum and simultaneous 3D resolution gains over conventional (circular pinhole based). This is realised with parameters $\alpha = 1.41$ and $\gamma = 1.00$. For any other parameter set chosen, the SNR of the differential pinhole system will always result in a lower SNR value than a conventional CFM system. However, it can be seen from figure 5(d), that the differential pinhole system outperforms (better SNR-resolution trade-off) the conventional system, with the optimum parameter set, in the axial direction for all SNR values. It should be noted that the graphs presented in figure 5 are calculated for NA = 0.5 and $\lambda = 0.5 \mu m$. However the threshold value of 0.63 quoted for these parameters does not change significantly for different parameters. For example for NA = 0.7 and $\lambda = 0.4 \mu m$, the threshold value changes to around 0.61.
Figure 4. ER based (a) lateral and (b) axial resolution contours for a constant SNR of 0.5. Minimas of the respective contours are found to be at \( \alpha = 1.41 \) and \( \gamma = 1.00 \). Here NA = 0.5 and \( \lambda = 0.5 \mu m \)

Figure 5. SNR versus resolution characteristics based on FWHM (plots (a) and (c)) and ER (plots (b) and (d)). Arrows indicate direction of increasing \( r_i \).
projection of which has an outer pinhole radius 0.6 \( \mu \)m respectively. Object consists of two fluorescent rings of width 0.5 \( \mu \)m, \( z_0 \) and the second a cross placed at ring structure placed at \( z_4 \). The resolution improvement can be clearly observed here.

Although absolute values are displayed in figure 6, as the total object function with the 2D confocal PSF in the plane of focus. The images have been generated by convolving the 2D uniform illumination. Shown are a series of sectioned images so that each emits the same mean number of photons for equal differential pinhole system, computer simulated images have been generated to show the imaging performance predicted for some simple object forms. The images presented in this section have been generated using the commonly-used paraxial and scalar imaging approximations [33], which allow the use of discrete Fourier transforms to convert pixelated representations of pupil functions to point-spread functions; convolution operations were also implemented through Fourier transformation, multiplication and inverse transformation using the \texttt{fft} function in MATLAB. The accuracy of the use of a Fourier optics approach has been discussed by a number of authors, see for example [34, 35]. Shot noise was modelled using the MATLAB Poisson noise generator \texttt{poissrnd}.

Figure 6 plots the absolute values of simulated images of an annular object as imaged by a circular pinhole CFM system (pinhole radius \( 0.4 \mu \)m) and a differential pinhole (circular projection of which has an outer pinhole radius \( 0.6 \mu \)m, \( \alpha = 1.41 \) and \( \gamma = 1 \)), with radii chosen to give the same SNR in both cases. The images have been generated by convolving the 2D object function with the 2D confocal PSF in the plane of focus. Although absolute values are displayed in figure 6, as the total PSF negative dip intensity is small, virtually identical images would be observed by just displaying the positive image intensities. The resolution improvement can be clearly observed here.

In figure 7, two planar objects are imaged—one an annular ring structure placed at \( z = 0 \) and the second a cross placed at \( z = 4 \mu \)m. Both the fluorescent objects have been normalised so that each emits the same mean number of photons for equal uniform illumination. Shown are a series of sectioned images as the focal plane of the illumination is moved between the two object planes. Owing to the tighter PSF mainlobe width and negligible negative sidelobes, the differential pinhole (circular projection of which has an outer pinhole radius \( 0.6 \mu \)m, \( \alpha = 1.41 \) and \( \gamma = 1 \)) based system compared to its circular pinhole counterpart (outer pinhole radius \( 0.4 \mu \)m, \( \alpha = 1 \) and \( \gamma = 0 \)) shows a greater separation of the two objects e.g. in the second image from the left in the top row the cross is still clearly visible in this image but in the lower image the cross is nearly invisible.

4. Image simulation results

To further illustrate the potential advantage of employing a differential pinhole system, computer simulated images have been generated to show the imaging performance predicted for some simple object forms. The images presented in this section have been generated using the commonly-used paraxial and scalar imaging approximations [33], which allow the use of discrete Fourier transforms to convert pixelated representations of pupil functions to point-spread functions; convolution operations were also implemented through Fourier transformation, multiplication and inverse transformation using the \texttt{fft} function in MATLAB. The accuracy of the use of a Fourier optics approach has been discussed by a number of authors, see for example [34, 35]. Shot noise was modelled using the MATLAB Poisson noise generator \texttt{poissrnd}.

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5. Conclusions

In this paper an optimum profile for the circular projection of an elliptically shaped differential pinhole has been deduced through the introduction of a new resolution metric, equivalent radius, which overcomes the inability of the conventional FWHM to take into account sidelobes in the PSF. For SNR <0.63 it has been shown that simultaneous resolution gains over a conventional circular pinhole geometry based CFM system, along both the lateral and axial directions can be obtained by setting the parameters \( \alpha = 1.41 \) and \( \gamma = 1 \) for the differential pinhole. In regard to the SNR-axial resolution trade-off, the differential pinhole system outperforms the conventional system, with the optimum parameter set, for all SNRs values. Requiring no significant modification to the CFM setup and using fast point detectors, the now optimised differential pinhole detection based CFM system offers significant 3D resolution gains at SNR <0.63. Although the new system carries a slightly increased overall implementation cost over a conventional circular pinhole geometry CFM system, the results show that images of considerably higher quality are produced.
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