Microlensing masses via photon bunching

Prasenjit Saha
Physik-Institut, University of Zurich, Winterthurerstrasse 190, 8057 Zurich, Switzerland

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ABSTRACT
In microlensing of a Galactic star by a brown dwarf or other compact object, the amplified image really consists of two unresolved images with slightly different light-travel times. The difference (of order a microsecond) is $G M/c^3$ times a dimensionless factor depending on the total magnification. Since magnification is well-measured in microlensing events, a single time-delay measurement would provide the mass of the lens, without degeneracies. The challenge is to find an observable that varies on sub-microsecond time scales. This paper notes that the narrow-band intensity of the unresolved image pair will show photon bunching (the Hanbury Brown and Twiss effect), and argues that the lensed intensity will have an auto-correlation peak at the lensing time delay. The ultrafast photon-counting technology needed for this type of measurement exists, but the photon numbers required to give sufficient signal-to-noise appear infeasible at present. Preliminary estimates suggest time-delayed photon bunching may be measurable for lensed early-type main-sequence stars at $\sim 10\,\text{kpc}$, with the help of 30 m-class telescopes.

Key words: gravitational lensing; micro - techniques: interferometric

1 INTRODUCTION
In Galactic microlensing there are two lensed images (more if the lens is binary), but there is no prospect of resolving them. Everything has to be inferred from a point image.

The principal observable is (i) the time-dependent brightness amplification (or light curve). Link (1936, 1937) and independently Einstein (1936) discussed it long before it became feasible to observe, with strikingly contrasting views on whether it could ever be observed. Later but still in the dream-time of gravitational lensing, Refsdal (1966a) drew attention to two more observables: (ii) parallax, which in the context of microlensing refers to the dependence of the light curve on observer location; and (iii) apparent proper motion of the image. Parallax depends on the spatial scale of the lens, while proper motion reveals its angular scale. Combining parallax and proper motion with the light curve yields the lens mass and distance. For parallax, Refsdal envisioned a spacecraft elsewhere in the solar system, an idea revived more recently (e.g., Boutreux & Gould 1999). For proper motions, Refsdal assumed that both source and lens would be visible stars. An alternative proposal, for when the lens is dark, is to monitor the lensed-image centroid for proper motion (e.g., Boden et al. 1998). Valis-Gabaud (1993, 1998) predicted a further observable: (iv) chromatic amplification, meaning colour, spectral and polarisation changes in the image due to variations of these across the face of the source star. Given a good model for the stellar atmosphere, chromatic amplification becomes in effect a surrogate for proper motion. Various observables come together beautifully in Gould et al. (2009), where chromatic amplification gives the angular scale, while the parallax is large enough to measure from different ground locations, and combined with the main light curve they supply the lens mass. But this cases are exceptional; as a rule, mass measurement in microlensing involves parameter degeneracies.

This paper will consider yet another possible observable in an unresolved microlensed image. This is the lensing time delay, or the difference in light travel time between the two lensed images. The formula for it is derived in Section 2 and comes to

$$\Delta t_{\text{lens}} = \frac{2GM}{c^3} \left( x^2 - 1/x^2 + 4 \ln x \right)$$

(1)

where

$$x^4 = \frac{A + 1}{A - 1}$$

(2)

and $A$ is the brightness amplification or total magnification. Since $A$ at any stage of a microlensing event is known accurately from the light curve, a single measurement of $\Delta t_{\text{lens}}$ would automatically measure the mass.

Time-delay measurements are an active area for galaxy and cluster lenses at cosmological distances (e.g., Rodney et al. 2016). There is also research on modelling the mass distributions of the lenses (as the point-mass approximation is not applicable to galaxies and cluster lenses) to infer cosmological parameters (e.g., Sereno & Paraficz 2014) or mass substructures (Mohammed et al. 2015). And
long before the first time-delay measurements, Refsdal (1964a, 1966b) was already advocating exploiting time-varying sources to measure time delays from galaxy lenses in order to measure cosmological parameters. Why then did he not propose time-delay measurements in his microlensing paper (Refsdal 1966a)? We can guess the reason: the scale of $\Delta t_{\text{mic}}$ is utterly different — microseconds for brown-dwarf lenses versus days to years for galaxy or cluster lenses — and stars are not known to have intrinsic brightness variations on sub-microsecond scales. Measuring microlensing time delays seems hopeless.

Yet perhaps not. Section 3 below will argue that fluctuations inherent in incoherent light (wave noise) could be used to advantage. The idea is to measure the brightness fluctuations, at any one stage of the microlensing event, with nanosecond time resolution. The photon statistics will then not be quite Poisson, but will show correlations. In particular, the auto-correlation of the photon arrival times will show the following features.

- First, there will be a peak at zero. This is the well-known phenomenon of photon bunching.
- Also expected — and this is the main prediction of this paper — are two smaller peaks at $\pm \Delta t_{\text{mic}}$, corresponding to the lensing time delay, or the difference in light travel time between the two lensed images.

Section 3 estimates the number of photons that would be needed to measure the secondary peaks in the intensity auto-correlation, assuming the effect is present. If nearby bright stars were microlensed, the auto-correlation peaks would be easy to measure. For stars at $\sim 10$ kpc, which is where most microlensed sources are, the necessary signal-to-noise appears unachievable at present. But upcoming developments (30 m telescopes, sub-nanosecond photon-counting arrays) could make the effect accessible for the brightest microlensed events.

2 MICROLENSING TIME DELAYS

To derive the expression (1) for the time delay in microlensing, let us consider the arrival-time surface (see e.g., Blandford & Narayan 1980). The arrival time, up to an additive constant, of a virtual photon coming from the direction $\theta$ but having originated at a source in the direction $\beta$ is

$$ct = \frac{D_L D_S}{2 D_{LS}} (\beta - \theta)^2 - \frac{4GM}{c^2} \ln \theta$$

where $D_L, D_S, D_{LS}$ are respectively the distances to the lens, source, and from lens to source. In terms of the angular Einstein radius

$$\theta_E^2 = \frac{4GM}{c^2} D_{LS}$$

the arrival time takes a cleaner form:

$$ct = \frac{4GM}{c^2} \left( \frac{(\beta - \theta)^2}{2\theta_E^2} - \ln \theta \right).$$

Actual photons take paths for which the arrival time is stationary, or $dt/d\theta = 0$. This condition gives the usual lens equation

$$\beta = \theta - \theta_E^2 / \theta.$$

Solutions of the lens equation can be conveniently written in terms of a new variable $x$ as

$$\theta = x \theta_E \text{ and } \theta = -\theta_E / x.$$  \hspace{1cm} (7)

The source position corresponding to both images is

$$\beta = (x - 1/x) \theta_E.$$ \hspace{1cm} (8)

Substituting the image and source positions into the arrival time (5) gives the value for each image. The difference between the arrival times of the two images then simplifies to the expression (1) for the time delay.

In order to relate $x$ to the brightness amplification, recall the well-known expression

$$\left( 1 - \frac{\theta_E}{\theta^2} \right)^{-1}$$

for the magnification due to a point lens. The absolute magnification at the two images comes to

$$A_1 = \frac{x^4}{x^4 - 1} \text{ and } A_2 = \frac{1}{x^4 - 1}$$

and the sum of these relates $x$ to the total magnification (Eq. 2).

Figure 1. A representation of the lensed images and arrival times for a solar-sized source in the lensing configuration (13). The middle panel shows the source while the other two panels show the lensed images. (The lens is at the origin.) The dots represent a quasi-random sample of 100 zones on the source. The grey-scale indicates the spread of arrival times within each image (darker for later arrival). The spread is $\Delta \Delta t_{\text{mic}} = 5$ ns for the earlier image, and 8 ns for the lower image. The systemic difference between the images is much more, with the lower image arriving $\Delta t_{\text{mic}} = 1584$ ns later on average.
The preceding applies only to a point source lensed by a point lens. For a realistic source, even an unresolved source, it is necessary to consider the effect of finite size. From the expressions \( 1 \) for the time delay and \( 8 \) for the source position, it follows that
\[
\frac{d}{d\beta}\Delta t_{\text{lens}} = \frac{4GM}{c^3} \frac{x + 1/x}{\theta_E} \tag{11}
\]
indicating that
\[
\frac{\Delta t_{\text{time}}}{\Delta t_{\text{lens}}} \approx \frac{\Delta \beta}{\theta_E} \tag{12}
\]
where \( \Delta t_{\text{time}} \) stands for the spread in time delays across the source. As an example, consider the configuration
\[
D_L = 4 \text{kpc} \quad D_S = 8 \text{kpc} \quad M = 0.08M_\odot \quad \beta = \frac{1}{2}\theta_E \tag{13}
\]
which would be typical of microlensing events. The projected Einstein radius will be \( D_L \theta_E = 1.1 \text{ au} \) at the lens, and \( D_S \theta_E = 2.2 \text{ au} \) at the source. If the source is Sun-sized, it will be much smaller than the projected Einstein radius, and the point-lens approximation is reasonable. Furthermore, \( \Delta t_{\text{lens}} \ll \Delta t_{\text{time}} \). The spread in time delays will, however, be orders of magnitude larger than the \( 1/\nu \) of light.

This is the reason lensed images do not produce interference fringes on the ground (cf. Refsdal 1964b, Press 1996). Figure \( 1 \) shows a numerical computation of arrival times from an extended source. We see that for a Sun-sized source in the lensing configuration \( 13 \), \( \Delta t_{\text{lens}} \approx 1.6 \times 10^{-9} \text{ s} \) and \( \Delta t_{\text{time}} \approx 10^{-8} \text{ s} \). We conclude that microlensing time delays could be measured if the light from the source has fluctuations that are faster than the microsecond scale, but not so fast that they average out within ten nanoseconds. The following section will argue that the desired fluctuations may be found in photon bunching.

3 PHOTON BUNCHING

Photon bunching, or the HBT effect (named after the pioneering experiments of Hanbury Brown & Twiss 1956), is a quantum-optical phenomenon, but can be studied semiclassically by first considering a complex wave and then interpreting the intensity of the wave as proportional to the probability of detecting photons.

Accordingly, let us consider the wave (a component of the electromagnetic field) for starlight in a narrow band \( S(\nu) \). The complex wave will then be
\[
E(t) = \int e^{2\pi i \nu t} S(\nu) d\nu, \tag{14}
\]
and the corresponding intensity will be
\[
I(t) \propto |E(t)|^2. \tag{15}
\]
If \( S(\nu) \) is a delta function, \( E(t) \) will just revolve in the complex plane at a constant rate and \( I(t) \) will be a constant. But if \( S(\nu) \) has a finite width, \( E(t) \) will have superpositions with random phases in the complex plane, making it like the endpoint of a random walk. Thus the probability distribution for \( E(t) \) will be Gaussian in the complex plane, and the intensity will have an exponential distribution. The larger the frequency spread in \( S(\nu) \) the more quickly \( E(t) \) and \( I(t) \) will sample their respective probability distributions. In particular, if \( S(\nu) \) is a Lorentzian
\[
S(\nu) \propto \frac{1}{1 + (2\pi \Delta \nu (\nu - \nu_0))^2} \tag{16}
\]
the time scale for the field and intensity to change will be \( \Delta \tau \). This is known as the coherence time. For a nanometre filter, the coherence time is roughly one picosecond. The intensity auto-correlation
\[
1 + g(\tau) \equiv \frac{\langle I(t) I(t + \tau) \rangle}{\langle I(t) \rangle^2} \tag{17}
\]
will have \( g(0) = 2 \) falling over a time \( \Delta \tau \) to \( g(\tau) = 1 \). This is the standard HBT effect.

Next we consider the effect of magnification by lensing. For an image magnified by say \( A_1 \), the intensity \( I(t) \) will get multiplied by \( A_1 \). The complex wave \( E(t) \) must get multiplied by \( \sqrt{A_1} \) times a phase factor. The multiplication by \( \sqrt{A_1} \) seems a little mysterious, but can be understood as follows. Recall that lensing magnification is the result of light rays, that would not have reached the observer without lensing, being deflected by the lens towards the observer. The corresponding complex waves add, but since they have random phases they add in random-walk fashion, which on average produces a factor of \( \sqrt{A_1} \).

Now consider a superposition of the waves from two lensed images. The intensity will be
\[
I(t) = \left| \sqrt{A_1} E(t) + \sqrt{A_2} E(t + \Delta t_{\text{lens}}) \right|^2 \tag{18}
\]
The waves \( E(t) \) and \( E(t + \Delta t_{\text{lens}}) \) are uncorrelated in phase, so there is no interference. The intensities, however, may be correlated. The auto-correlation \( 17 \) are expected to show secondary peaks of height \( A_1 A_2/(A_1 + A_2) \), or
\[
g(\pm \Delta t_{\text{lens}}) = \frac{A_1^2 - 1}{4A_1} \tag{19}
\]
in addition to the main peak of \( g(0) = 1 \).

Figure 2 shows a simulation of lensed intensity and auto-correlation, obtained as follows.

(i) Each of the 100 zones in Figure 1 is taken to emit a wave \( E(t) \) having a Lorentzian spectral profile with \( \Delta = 10^{-8} \text{ s} \). The central frequency \( \nu_0 \) makes no difference to the intensity and is set to zero, but the wave from each zone is given a random initial phase. The simulated time duration is a millisecond, of which only \( \approx 8 \) microseconds is shown in the figure.

(ii) Each wave is lensed in the same lensing configuration as in Figure 1. That is, each wave is delayed by the appropriate amount and multiplied by \( \sqrt{A_1} \) or \( \sqrt{A_2} \).

(iii) All the waves are added, and the intensity computed.

(iv) Finally the intensity is auto-correlated. Expected are a central peak rising to 2, and (in the assumed lensing configuration) secondary peaks at \( \pm 1.6 \) microsec, each rising to 1.2.

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1 This was first shown by Sudarshan 1962 and is nowadays called the optical equivalence theorem.

2 The precise definition of coherence time varies in the literature. This work follows \( \Delta \tau \) from Mandel & Wolf (1962).
Note that there is no shot noise in Figure 2. The intensity fluctuations are just a property of narrow-band light. They are well-known in radio astronomy as wave noise (Radhakrishnan 1999). Photon counts will follow a Poisson distribution with the intensity varying over a time-scale of $\Delta \tau$. The result is photon bunching. The term ‘super-Poisson noise’ is also used.

The secondary peaks in the auto-correlation are very interesting — but are the arguments and simulation valid? There are at least three possible concerns.

1. First, it is surprising that the intensity auto-correlation appears not to depend on $\nu_0$, only on $\Delta \nu$.
2. Second, there is the assumption that the source can be expressed as the sum of small zones. The simulation is not sensitive to the number of zones. On the other hand, the sample points representing zones are $\sim 0.5$ light-sec part, which is an order of magnitude larger than the Fresnel-zone length $\sqrt{\lambda D_s}$ associated with diffraction. Actually, diffraction effects are possible on even smaller scales, though only near lensing caustics (e.g., Zabel & Peterson 2003) which does not apply to most microlensing events.
3. Third, the factors of $\sqrt{A_1}$ and $\sqrt{A_2}$ in the total intensity $I$ would come with arbitrary phases; but again, these would not destroy the auto-correlation.

A laboratory experiment to test for time-delayed photon bunching is desirable. A suitable variant of the experiments by Dravins et al. (2013) and Tan et al. (2016) could do such a test.

4 SIGNAL-TO-NOISE CONSIDERATIONS

Assuming time-delayed photon bunching is real, identifying the most promising events in advance would not be a problem. Although Galactic microlensing events are rare, with at most a few stars per million being lensed at any given time (Sumi et al. 2013), an early-warning system (such as in Udalski et al. 2013) would provide the expected image brightness and magnification. The challenge would be getting sufficient signal-to-noise to measure the time-delayed photon bunching on even the best candidates.

The basic setup and signal-to-noise considerations would be similar to those in recent work on intensity interferometry (Pilyavsky et al. 2017, Lai et al. 2018, Weiss et al. 2018). The starlight is filtered to a very narrow wavelength band, to increase the coherence time $\Delta \tau$, and then photons are counted with a time-resolution $\Delta t$. The Favoured detector technology is single-photon avalanche photodiodes. Multiple photodiodes, each devoted to one narrow wavelength range, can be used in parallel, thus having multiple photon-counting channels.

In intensity interferometry there are two (or more) telescopes whose photon counts are cross-correlated, whereas for microlensing only one telescope is required — but a bigger one, because the targets are fainter. An additional requirement in microlensing is to have the coherence time $\Delta \tau$ comparable to or longer than the time-delay spread $\Delta \Delta \tau_{\text{lens}}$.

The latter condition could be checked in advance, since an approximate source size $\Delta \beta$ would be available for an ongoing microlensing event, providing ballpark estimates for $\Delta \tau_{\text{lens}}$ and $\Delta \Delta \tau_{\text{lens}}$.

The SNR can be estimated by adapting an argument from intensity interferometry, as follows. Let $r$ be the rate of photons arriving per unit collecting area in some narrow spectral band, and let $\Delta \tau \sim 1/\Delta \nu$ be the coherence time corresponding to that spectral band. If the telescope has unit collecting area and perfect detection efficiency, the number of photons per coherence time will be $r \Delta \tau$. Now consider two time bins, each of duration $\Delta t$ (the instrumental time resolution), but separated by $\Delta \Delta \tau_{\text{lens}}$.

- Each time bin will contain $\Delta \tau/\Delta \Delta \tau$ time slices, during which the light is coherent. In a pair of coherent time slices $\Delta \Delta \tau_{\text{lens}}$ apart, there will be $g(\Delta \tau_{\text{lens}}) \times (r \Delta \tau)^2$ pairs of HBT-correlated photons. Hence, there will be $g(\Delta \tau_{\text{lens}}) \times r^2 \Delta \tau \Delta \Delta \tau_{\text{lens}}$ HBT-correlation events per time bin. This is the signal.
- Meanwhile in the same time bins, there will $(r \Delta t)^2$ pairs of photons correlated by chance. This number is the background, and $r \Delta t$ is the corresponding noise.

The SNR per time bin $\Delta t$ is thus $g(\Delta \tau_{\text{lens}}) \times r \Delta \tau$. This applies to unit collecting area and perfect detectors. If we have collecting area $A$ and photon-detection efficiency $\gamma$, these factors just multiply $r$. Concerning the spectral bandpass, narrowing it reduces $r$ but increases $\Delta \tau$ by the same factor, and (remarkably) leaves the SNR per time bin unaffected. Hence, it is advantageous to have many narrow spectral channels. For $N$ channels, the SNR gets multiplied by $\sqrt{N}$. Similarly, if the total observing time is $T$, the SNR will be multiplied by $\sqrt{T/\Delta \Delta \tau_{\text{lens}}}$. The result is

$$\text{SNR} \sim g(\Delta \tau_{\text{lens}}) \times \gamma A \tau \Delta \tau \left( \frac{N T}{\Delta \Delta \tau_{\text{lens}}} \right)^{1/2}$$  \hspace{2cm} (20)$$

provided $\Delta t \gtrsim \Delta \tau$. The SNR improves as the time resolution gets smaller, until it becomes comparable to the coherence time. Lowering $\Delta \tau$ still further does not help, as super-Poisson noise takes over (Malvimat et al. 2014). The factor $g(\Delta \tau_{\text{lens}})$ will be less than one, but roughly compensating for that is the increase in $r$ from lensing amplification. So it is reasonable to consider $(\gamma A) \times (r \Delta \tau) \times \sqrt{N T/\Delta \Delta \tau_{\text{lens}}}$ without lensing.

To reach a reasonable SNR in one night, one would need to achieve $\text{SNR} \sim 1$ in $T = 10^5 \text{s}$. If $N = 10$ channels each with $\Delta t = 10^{-8} \text{s}$ are installed, $\sqrt{N T/\Delta \Delta \tau_{\text{lens}}} \sim 10^6$. Hence one
needs $(\gamma_A) \times (r \Delta \tau) \sim 10^{-6}$ at least. The next generation of extremely large telescopes and highly efficient detectors could offer $\gamma_A \sim 10^5 \text{ s}^{-1}$ at best. This suggests that sources down to $r \Delta \tau \sim 10^{-9} \text{ m}^{-2}$ would be plausible targets.

The photon flux per coherence time $r \Delta \tau$ is simply the spectral flux density divided by energy and integrated over the source. Figure 3 shows some example curves of $r \Delta \tau$. A blackbody disc of radius $R_\odot$ and $T = 5800 \text{ K}$, viewed from 1 pc is labelled “Sun”. A disc of radius 0.2$R_\odot$ and $T = 3100 \text{ K}$ viewed from the same distance is labelled “Barnard’s star”. Similarly, the label “Sirius” corresponds to 9$R_\odot$ and $T = 15000 \text{ K}$ from 1 pc. From such a short distance, any of these would be a plausible candidate. But if they are located at $\sim 10 \text{ kpc}$, the value of $r \Delta \tau$ falls by a factor of 10$^6$. This leaves only “Achernar” as a plausible candidate.

The above suggests that photon bunching would be measurable in O or B main-sequence stars at $\sim 10 \text{ kpc}$. (Giants or supergiant stars of similar brightness are unlikely to be useful, because $\Delta \beta$ will become comparable to $\theta_E$, washing out the time-delay peaks.) Microlensed early-type stars must be exceedingly rare, and it is not clear that any have been observed yet. Nataf et al. (2000) show some candidate light curves in their Figure 5, which may have been such, if they were indeed microlensing events.

Plans for intensity interferometers include proposals to create light buckets as large as $10^4 \text{ m}^2$ by attaching additional detectors to air Cerenkov telescopes (Dravins 2016). The mirrors involved are not optical quality (hence the huge areas). These sacrifice image quality but remain adequate for collecting light from bright stars. Microlensing surveys, however, need to target crowded fields of stars, and to count photons from a single star in a crowded field, good image quality is essential. Hence a general-purpose telescope cannot be substituted, and there is no way of increasing $A$ in Eq. (20) in the near future. Any hope for increased sensitivity would lie in increasing the number of spectral channels $N$. Small arrays of single-photon avalanche photodiodes have been tested (e.g., Tosi et al. 2014), and perhaps much larger arrays may be possible in the future. Another class of detectors with prospects for many-channel photon counting are superconducting nanowires (e.g., Verma et al. 2015).

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