Double fermiophobic Higgs boson production at the LHC and LC

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Abstract

We consider the phenomenology of a fermiophobic Higgs boson ($h_f$) at the Large Hadron Collider (LHC) and a $e^+e^-$ Linear Collider (LC). At both machines the standard production mechanisms which rely on the coupling $h_fVV$ ($V = W^\pm, Z$) can be very suppressed at large $\tan\beta$. In such cases the complementary channels $pp \rightarrow H^\pm h_f, A^0 h_f$ and $e^+e^- \rightarrow A^0 h_f$ offer promising cross-sections. Together with the potentially large branching ratios for $H^\pm \rightarrow h_f W^*$ and $A^0 \rightarrow h_f Z^*$, these mechanisms would give rise to double $h_f$ production, leading to signatures of $\gamma\gamma\gamma\gamma, \gamma\gammaVV$ and $VVVV$. 
1 Introduction

Neutral Higgs bosons ($h^0$) with branching ratios (BRs) very different to those of the Standard Model (SM) Higgs boson, $\phi^0$, can arise in extensions of the SM which contain an additional $SU(2) \times U(1)$ Higgs doublet, the “Two Higgs Doublet Model” (2HDM) [1]. Assuming that each fermion type (up/down) couples to only one Higgs doublet [2], which eliminates tree-level Higgs mediated flavour changing neutral currents, leads to 4 distinct versions of the 2HDM [3]. No compelling experimental evidence has been found for Higgs bosons. Experimental searches for $\phi^0$ at LEP concentrated on the channel $\phi^0 \rightarrow b\bar{b}$ [4], while more recently [5] searches for Higgs bosons with large branching ratios (BRs) to lighter fermions and gluons (i.e. $c\bar{c}, \tau^+\tau^-, gg$ [6]) were performed. The phenomena known as “fermiophobia” [7] which signifies very suppressed or zero coupling to the fermions, may arise in a particular version of the 2HDM called type I [8] or in models with Higgs triplets [9]. Depending on its mass, a fermiophobic Higgs ($h_f$) [10, 11, 12, 13, 14, 15, 16] would decay dominantly to two photons, $h_f \rightarrow \gamma\gamma$, for $m_{h_f} < 95$ GeV or to two massive gauge bosons, $h_f \rightarrow VV^{(*)}$, ($V = W^\pm, Z$) if $m_{h_f} > 95$ GeV [12, 13]. The large BR to $\gamma\gamma$ would give a very clear experimental signature, and observation of such a particle would strongly constrain the possible choices of the underlying Higgs sector.

Experimental searches for fermiophobic Higgs bosons at LEP and Fermilab have been negative so far. Lower bounds of the order $m_{h_f} \geq 100$ GeV have been obtained by the LEP collaborations OPAL [18], DELPHI [19], ALEPH [20], and L3 [21], utilizing the channel $e^+e^- \rightarrow h_fZ$, $h_f \rightarrow \gamma\gamma$. Only L3 [22] has considered $h_f \rightarrow WW^*$ decays. OPAL [18] and DELPHI [19] also searched in the channel $e^+e^- \rightarrow h_fA^0$, $h_f \rightarrow \gamma\gamma$. From the Tevatron Run I, the limits on $m_{h_f}$ from the D0 and CDF collaborations are respectively 78.5 GeV [23] and 82 GeV [24] at 95% c.l., using the mechanism $qq' \rightarrow V^* \rightarrow h_fV, h_f \rightarrow \gamma\gamma$, with the dominant contribution coming from $V = W^\pm$. Run II will extend the coverage of $m_{h_f}$ beyond that of LEP [25, 26].

All the above mass limits, however, assume that the $h_fVV$ coupling is of the same strength as the SM coupling $\phi^0VV$, which in general would not be the case for a $h_f$ in a realistic model in which the $h_fVV$ coupling has an additional suppression from a mixing angle. Such a scenario would enable a very light $h_f$ ($m_{h_f} << 100$ GeV) to escape the searches at LEP and the Tevatron Run I. Therefore it is of interest to consider other production mechanisms for $h_f$ which may still allow observable rates even when the $h_fVV$ coupling is suppressed. In a previous paper [27] we proposed several new production mechanisms at the Tevatron Run II. In particular, the process $p\bar{p} \rightarrow H^{\pm}h_f$ offers promising rates if the masses of both $H^\pm$ and $h_f$ are less than 100 GeV. These complementary mechanisms cover some of the region of suppressed coupling $h_fVV$, particularly if $m_{h_f} < 80$ GeV. However, for heavier $m_{h_f}$ (> 80 GeV), detection prospects are diminished due to phase space suppression at the Tevatron energy. In this paper we extend the analysis of [27] to consider the search potential at two future colliders, the Large Hadron Collider (LHC) and a $e^+e^-$ Linear Collider (LC). These colliders will offer significantly improved detection prospects for $h_f$, and in case of a $h_f$ being detected in Run II would allow a more precise determination of its properties. Our work is organised as follows. In Section 2 we
give a brief introduction to fermiophobic Higgs bosons. Section 3 covers the production of \( h_f \) at the LHC and LC, while Section 4 contains our numerical results. Conclusions are given in Section 5.

# 2 Fermiophobic Higgs bosons

The first studies of the phenomenology of \( h_f \) can be found in [10],[11]. BRs for \( h_f \) were presented in [12],[13] while its phenomenology at the Tevatron Run I was covered in [12],[14]. Production at LEP2 and the impact of charged scalar loops on BR(\( h_f \to \gamma\gamma \)) (mediated via the trilinear coupling \( h_f H^+ H^- \)) were studied in [15],[16].

Such a particle may arise in a 2HDM in which one \( SU(2) \times U(1) \) Higgs doublet (\( \Phi_2 \)) couples to all fermion types, while the other doublet (\( \Phi_1 \)) does not. This model is usually called “Type I” [8]. Due to the mixing in the CP–even neutral Higgs mass matrix (which is diagonalized by \( \alpha \)) both CP–even eigenstates \( h^0 \) and \( H^0 \) can couple to the fermions. The fermionic couplings of the lightest CP–even Higgs \( h^0 \) take the form \( h^0 f \bar{f} \sim \cos \alpha / \sin \beta \), where \( f \) is any fermion and \( \beta \) is defined by \( \tan \beta = v_2 / v_1 \) (where \( v_i \) is the vacuum expectation value of the \( i \)th doublet). Small values of \( \cos \alpha \) would strongly suppress the fermionic couplings, and in the limit \( \cos \alpha \to 0 \) the coupling \( h^0 f \bar{f} \) would vanish at tree–level, giving rise to fermiophobia,

\[
\begin{align*}
\h_f & \, \longrightarrow \, \h_f f \bar{f} \\
& = \frac{\cos \alpha}{\sin \beta} \sim 0.
\end{align*}
\]

Exact tree level fermiophobia is not stable under radiative corrections [13],[15]. One can estimate what sort of deviation from exact fermiophobia we could expect by considering as an example the quantum correction involving two \( W \). To estimate the order of magnitude of this correction we approximate

\[
\begin{align*}
\Delta g_{h_f f \bar{f}} & \sim \frac{1}{16\pi^2} (g m_W) (\frac{q^2}{8}) m_f C(m_h, \phi, 0, 0; m_W, m_W^2)
\end{align*}
\]

where \( C \) is a generic triangular Veltman’s function. If we approximate \( C \sim 1/m_h^2 \), expected in the limit of large Higgs mass, and compare this correction with the tree level vertex in the SM \( g_{h_f f \bar{f}} \sim g m_f / 2 m_W \) we find,

\[
\frac{\Delta g_{h_f f \bar{f}}}{g_{h_f f \bar{f}}} \sim \frac{g^2}{64\pi^2} \left( \frac{m_W}{m_h} \right)^2 \sim 10^{-4}
\]

(1)
for a Higgs mass twice as large as the $W$ mass. This indicates that tree-level fermiophobia is weakly affected by quantum corrections.

In general one would expect approximate fermiophobia, with some small coupling to fermions:

\[
  h_f \sim 0
\]

Of course, the correct renormalization of this vertex involves counterterms that need to be fixed with experimental measurements. We mention two examples in the literature on how this counterterm can be fixed. In the first example [16] the authors set $\cos \alpha = 0$ at tree level, i.e., tree-level fermiophobia. In this case, the one-loop contributions to the $h_f f \bar{f}$ coupling are finite and therefore the counterterm is finite as well. The finite part of the counterterm is also chosen to be zero, such that the renormalized coupling becomes equal to the sum of the finite one-loop graphs that contribute to it. In this scheme, $\cos \alpha = 0$ means tree-level fermiophobia, and at one-loop the coupling $h_f f \bar{f}$ is not zero, although small, inducing a small $h_f \rightarrow b \bar{b}$ branching ratio as observed in their figures.

In the second example [17], the authors are concerned with the 1-loop fermionic decay width in the context of the 2HDM (Model II), but nevertheless their results can be adapted to the case of $h_f$ in the 2HDM (Model I). In [17] the counterterm for the angle $\alpha$ is chosen such that there is no mixing between $h$ and $H$. This means that $\alpha$ is the mixing angle at one-loop implying that the one-loop coupling $h_f f \bar{f}$ is proportional to $\cos \alpha$, as can be seen from their formula for the decay width to fermions. In this scheme, $\cos \alpha = 0$ means one-loop fermiophobia, and therefore the definitions for $\alpha$ in the two schemes are not equivalent, and a relation between the two parameters $\alpha$ must be derived in order to compare.

The main decay modes of a fermiophobic Higgs are $h_f \rightarrow \gamma \gamma, W^* W^*, Z^* Z^*$. Assuming that $h_f \rightarrow \gamma \gamma$ is primarily mediated by the $W$ loop, this photonic channel is dominant for $m_{h_f} \lesssim 95$ GeV, with a BR near 100% for $m_{h_f} \lesssim 80$ GeV, decreasing to 50% at $m_{h_f} \approx 95$ GeV and to 1% at $m_{h_f} \approx 145$ GeV. In contrast, $\text{BR}(\phi^0 \rightarrow \gamma \gamma) \approx 0.22\%$ is the largest value in the SM, occurring around $m_{\phi^0} = 120$ GeV. The photonic decay mode is a particularly robust sign of fermiophobia for $m_{h_f} \leq 150$ GeV, above which $\text{BR}(h_f \rightarrow \gamma \gamma)$ approaches the SM value. Fermiophobic models permit the largest BRs to two photons, but (smaller) enhancements relative to the SM BR are also possible in other models where a neutral Higgs boson ($h^0$) couples to some but not all quarks, either by choosing appropriate mixing angles [33], or as a consequence of model building [25], [34]. Enhancements of $\text{BR}(h^0 \rightarrow \gamma \gamma)$ due to the scalar loop contribution were studied in [17],[35] in the decoupling limit of the 2HDM (Model II). In this paper we will focus on $h_f$ from the 2HDM (Model I).
3 \( h_f \) production at LHC and LC

In this section we consider the production of \( h_f \) at the LHC and LC, in both the standard mechanisms (which depend on the \( h_f VV \) coupling), and the complementary mechanisms which produce \( h_f \) together with another Higgs boson, and depend on the \( h_f HV \) coupling with \( H = H^\pm \) or \( A^0 \). For studies of these complementary mechanisms in the context of models without a \( h_f \), see [36]. We will present the cross-sections as a function of \( m_{h_f}, \tan \beta \) and \( m_{H^\pm}/m_A \). Our analysis can be applied to two different scenarios:

(i) \textit{Detection} of a \( h_f \) at the Tevatron Run II. In this case the LHC and LC would provide confirmation as well as further studies of the \( h_f \) properties.

(ii) \textit{Non-observation} of a \( h_f \) at the Tevatron Run II. In this case the LHC and LC would probe a significantly larger parameter space of \( m_{h_f} \) and \( \tan \beta \).

In the case of \( h_f \) production at \( e^+ e^- \) colliders, the complementary mechanism has been exploited at LEP [18],[19] which searched for \( e^+ e^- \to A^0 h_f \). So far, complementary mechanisms have not been considered at the Tevatron. As emphasized in [27], a more complete search strategy for \( h_f \) at Hadron colliders would include such production processes.

3.1 Standard mechanisms

At the LHC there are two standard ways to produce \( h_f \), for which experimental simulations have been performed in the context of the SM Higgs boson (\( \phi^0 \)). These are:

(i) \( pp \to W^* \to Wh_f, W \to l\nu \) (Higgsstrahlung) [28]

(ii) \( pp \to qqh_f \) (Vector boson fusion) [29],[30]

At a \( e^+ e^- \) LC one has the following mechanisms:

(iii) \( e^+ e^- \to h_f Z \) (Higgsstrahlung) [31]

(iv) \( e^+ e^- \to h_f \nu \bar{\nu} \) (W boson fusion) [31]

All the above mechanisms have been shown to be effective for \( \phi^0 \) due to its substantial coupling to vector bosons (for a recent application of the above processes to \( h^0 \) of the MSSM see [32]). This is not necessarily the case in the 2HDM, in which a \( h_f \) may arise. In the 2HDM the mechanisms (i) to (iv) for \( h_f \) are all suppressed by \( \sin^2(\beta - \alpha) \), which in the tree-level fermiophobic limit (\( \alpha \to \pi/2 \)) in Model I simplifies to:

\[
VVh_f \sim \cos^2 \beta \quad (\equiv 1/(1 + \tan^2 \beta))
\]  \hspace{1cm} (2)

This is a severe suppression for \( \tan \beta \geq 10 \) and renders all the above mechanisms unobservable (for an earlier discussion with just mechanism (i) see [33]). This is shown
Figure 1: Signal/Background ratio for a fermiophobic Higgs $h_f$ decaying into two photons, as a function of $\tan \beta$. Two production mechanisms are considered at the LHC and two at a future LC ($\sqrt{s} = 500$ GeV).
in Fig.1, where we apply the results of the signal/background \( \left( \frac{S^0}{\sqrt{B}} \right) \) simulations for \( \phi^0 \rightarrow \gamma \gamma \) to the case of a \( h_f \). To do this we need to scale the SM Higgs signal \( S^0 \) by the factor \( \frac{BR(h_f \rightarrow \gamma \gamma)}{BR(\phi^0 \rightarrow \gamma \gamma)} \), and include the \( \cos^2 \beta \) suppression in the production cross-sections. Our aim is to merely show the strong dependence of \( S/\sqrt{B} \) on \( \tan \beta \). We show results for \( S/\sqrt{B} > 1 \) and are not concerned with additional statistical and systematic considerations associated with small signal rates. Since all the above simulations presented results for \( m_{\phi^0} = 120 \text{ GeV} \) we will consider a \( h_f \) of this mass. For \( m_{h_f} = 120 \text{ GeV} \) one has \cite{12}, \cite{13}:

\[
BR(h_f \rightarrow \gamma \gamma)/BR(\phi^0 \rightarrow \gamma \gamma) \approx 10
\]  

(3)

In Fig.1 we plot \( S/\sqrt{B} \) for \( h_f \) as a function of \( \tan \beta \). We include the production mechanisms (i)-(iv) and take \( m_{h_f} = 120 \text{ GeV} \). For mechanism (ii) we use the results of the simulation in \cite{30}. Each curve is of the simple form:

\[
S/\sqrt{B} = 10 K_i \cos^2 \beta
\]  

(4)

where \( K_i \) \( (i = 1, 4) \) corresponds to the SM Higgs \( S^0/\sqrt{B} \) for each of the mechanisms (i)-(iv). We assume luminosities (\( \mathcal{L} \)) of 50 fb\(^{-1} \) for (i),(ii) and 1000 fb\(^{-1} \) for (iii),(iv). For other choices of \( \mathcal{L} \) the \( S/\sqrt{B} \) scales as \( \sqrt{\mathcal{L}} \). One can see that all the mechanisms offer spectacular signals \( (S/\sqrt{B} >> 5) \) when there is little suppression in the cross-section at low \( \tan \beta \). However, \( S/\sqrt{B} \) falls rapidly as \( \tan \beta \) increases, and \( S/\sqrt{B} < 5 \) at some critical value \( \tan \beta_C \). In Fig.1, \( \tan \beta_C \) varies between 2 and 5. Hence unless \( \tan \beta \) is fairly small a relatively light \( h_f \) (even \( m_{h_f} << 120 \text{ GeV} \)) may escape detection at both the LHC and LC.

### 3.2 Complementary mechanisms

Complementary mechanisms play an important role in the search for \( h_f \) in the case of the \( h_fVV \) coupling being suppressed. The process \( pp \rightarrow H^\pm h_f \) \cite{27} at the Tevatron Run II, although offering promising rates for lighter \( m_{h_f} \) is significantly suppressed for \( m_{h_f}, m_{H^\pm} > 100 \text{ GeV} \). We shall consider the following direct production mechanisms of \( h_f \),

(i) At the LHC: \( pp \rightarrow H^\pm h_f, A^0 h_f \)

(ii) At a LC: \( e^+e^- \rightarrow A^0 h_f \)
We are not aware of explicit signal–background simulations for these channels. Mechanism (i) is expected to be ineffective for decays of Higgs bosons to fermions, but for the case of $h_f \rightarrow \gamma\gamma$ might offer more promising detection prospects. Mechanism (ii) is the LC analogy of the LEP2 process, and is usually absent in discussions of the MSSM Higgs bosons due to the strong suppression of $\cos^2(\beta - \alpha)$ for $m_A \geq m_Z$ in such models. However for a $h_f$ in the region of suppressed $h_f VV$ coupling it offers promising rates. Detection prospects for $e^+ e^- \rightarrow A^0 h_f, h_f \rightarrow \gamma\gamma$ at larger $\tan \beta$ might be comparable to those for the Higgsstrahlung channel $e^+ e^- \rightarrow Z h_f$ at low $\tan \beta$ (see Fig.1).

The cross-section formulae for all the processes can be found in [37],[38]. They depend on three input parameters, $m_{h_f}, \tan \beta$ and one of $m_A, m_{H^\pm}$. We sum over $\sigma(pp \rightarrow H^+ h_f)$ and $\sigma(pp \rightarrow H^- h_f)$.

### 3.3 Decays $H^\pm \rightarrow h_f W^*$ and $A^0 \rightarrow h_f Z^*$

The experimental signature arising from the complementary mechanisms in section 3.2 depends on the decay products of $H^\pm$ and $A^0$. It has been shown [39] (see also [40]) that both $BR(H^\pm \rightarrow h_f W^*)$ and $BR(A^0 \rightarrow h_f Z^*)$ can be very large in the 2HDM (Model I) since the decay widths to the fermions $(H^\pm \rightarrow f\bar{f}, A^0 \rightarrow f\bar{f})$ scale as $1/\tan^2 \beta$. Thus in the region of $\tan \beta > 10$ (where the complementary mechanisms are important) the fermionic channels are very suppressed, enabling the decays $H^\pm \rightarrow h_f W^*$ and $A^0 \rightarrow h_f Z^*$ to become the dominant channels. Ref.[39] studied the BRs for Higgs boson masses of interest at LEP2. In this paper we are extending their analysis to include masses of interest at the LHC and a LC.

In Fig. 2 we plot curves of constant charged Higgs branching ratio in the $m_{h_f} - \tan \beta$ plane for $m_{H^\pm} = 150$ GeV. The solid curves correspond to $BR(H^\pm \rightarrow W^* h_f)$ and the dashed lines correspond to $BR(H^\pm \rightarrow \tau\nu)$. The decay that interests us here, $H^\pm \rightarrow W^* h_f$, dominates at low values of $m_{h_f}$ because in this case $W^*$ is more on-shell; it also dominates at large values of $\tan \beta$ because the competing $H^\pm f\bar{f}$ decays are suppressed by $1/\tan^2 \beta$. In contrast, the decay $H^\pm \rightarrow \tau\nu$ dominates at large values of $m_{h_f}$ and small values of $\tan \beta$. For $m_f > 150$ GeV, the fermiophobic Higgs is no longer real.

Fig. 3 is a similar plot where we have curves with constant CP-odd Higgs branching ratios in the $m_{h_f} - \tan \beta$ plane for $m_A = 150$ GeV. As in the previous figure, $BR(A^0 \rightarrow Zh_f)$ is in solid lines and dominates when $m_{h_f}$ is small and $\tan \beta$ is large, and $BR(A^0 \rightarrow b\bar{b})$ is in dashed lines and dominates when $m_{h_f}$ is large and $\tan \beta$ is small. By comparing
Figure 2: Curves with constant branching ratios $BR(H^\pm \to W^*h_f) = 0.5$, 0.9, and 0.99, and $BR(H^\pm \to \tau \nu) = 0.5, 0.65$, and 0.9, in the $m_{h_f} - \tan \beta$ plane for $m_{H^+} = 150$ GeV.
Figure 3: Curves with constant branching ratios $BR(A^0 \rightarrow Z^* h_f) = 0.5, 0.9, \text{ and } 0.99, \text{ and } BR(A^0 \rightarrow b\bar{b}) = 0.5, 0.75, \text{ and } 0.9,$ in the $m_{h_f} - \tan \beta$ plane for $m_A = 150$ GeV.
Figs. 2 and 3 it is apparent that the region of domination of the decay $A^0 \to \gamma \gamma$ is smaller than that for the decay $H^\pm \to W^+ h_f$. This is because the decay width for $A^0 \to \gamma \gamma$ is larger than that for $H^\pm \to \tau \nu$, since the former $\sim m_h^2$ while the latter $\sim m_{\tau}^2$.

In the lower regions of $m_{hf} - \tan \beta$ parameter space where $BR(H^\pm \to W^* h_f) > 0.5$ and $BR(A^0 \to \gamma \gamma) > 0.5$, a directly produced fermiophobic Higgs boson may be accompanied by one produced indirectly from the decay of $H^\pm$ or $A^0$. This scenario would give rise to double $h_f$ production, with subsequent decay of $h_f h_f \to \gamma \gamma \gamma \gamma$, $V V \gamma \gamma$ and $V V V V$. For light $h_f$ ($m_{hf} < 80$ GeV), the signal $\gamma \gamma \gamma \gamma$ would dominate, as discussed in [39] at LEP, and in [27] for the Tevatron Run II. For $m_{hf} \approx 95$ GeV the channels $V V \gamma \gamma$ and $V V V V$ would be comparable in number to $\gamma \gamma \gamma \gamma$, while for $m_{hf} > 100$ GeV, the $V V V V$ would start to be the dominant signature. We stress that double $h_f$ production requires a large $BR(H^\pm \to h_f W^*)$ or $BR(A^0 \to h_f Z^*)$ and is a feature of the 2HDM (Model I). The analogous BRs in other versions of the 2HDM are much smaller, although large BRs are also possible in triplet models with fermiophobia [41].

4 Production Cross Sections

For the production cross–sections at the LHC we shall be using the MRST2002 set from [42]. Note that QCD corrections increase the tree–level cross–section by a factor of around 1.3 [38]. In our analysis we shall present results using the tree–level formulae only. In the following figures we plot contour lines of constant cross–section at both the LC and LHC for different choices of parameters $m_{hf}, \tan \beta, m_{H^\pm}, A^0$. We will show results for $e^+e^- \to h_f A^0$ and $pp \to H^\pm h_f$. The cross–section for $pp \to h_f A^0$ is half that of $pp \to H^\pm h_f$, for $m_A = m_{H^\pm}$.

In Fig. 4 we have contours of constant production cross section at the LC with $\sqrt{s} = 500$ GeV in the $\tan \beta - m_{hf}$ plane, where $m_{hf}$ is the fermiophobic Higgs boson mass. The four dashed lines correspond to the standard production mechanism $e^+e^- \to \gamma \gamma$, with its cross section being equal to $\sigma(Z h_f) = 20, 25, 30$, and $35$ fb. The four solid lines correspond to the complementary mechanism $e^+e^- \to A^0 h_f$ with the same values for its cross section $\sigma(A^0 h_f)$, and taking $m_A = 150$ GeV. The higgsstrahlung production mechanism dominates at small $\tan \beta$ since, in this model, the cross section is proportional to $\cos^2 \beta$ (as explained in Section 3.1). On the contrary, the production of a fermiophobic Higgs in association with a CP-odd Higgs $A^0$ dominates at large $\tan \beta$ due to the dependence of the cross section on $\sin^2 \beta$. For this reason, in the case of $\sigma(Z h_f)$ the constant cross section contours strongly depend on $\tan \beta$, and for $\tan \beta \lesssim 2$ the cross section is already smaller than $20$ fb. Equally sharp but opposite dependence on $\tan \beta$ is observed for the constant $\sigma(A^0 h_f)$ contours. This effect is evident as a clear depression of the observability of $h_f$ at around $\tan \beta = 1-2$, where both cross sections are smaller than $20$ fb for $m_{hf} \gtrsim 130$ GeV.

In Fig. 5 we have similar contours of constant production cross section, but this time at the LHC with $\sqrt{s} = 14$ TeV, in the $\tan \beta - m_{hf}$ plane. The four dashed lines correspond
Figure 4: Curves with constant production cross section $\sigma = 20, 25, 30,$ and 35 fb at a future LC in the $m_{h_t} - \tan \beta$ plane for $m_A = 150$ GeV.
Figure 5: Curves with constant production cross section $\sigma = 70, 100, 130, \text{ and } 160 \text{ fb} \text{ at the LHC in the } m_{h_f} - \tan \beta \text{ plane for } m_{H^+} = 150 \text{ GeV}.$
Figure 6: *Curves with constant production cross section $\sigma = 20$, 25, 30, and 35 fb at a future LC in the $m_{h_f} - m_A$ plane for $\tan \beta = 20$.**

to the standard mechanism $pp \rightarrow Wh_f$ with values $\sigma(Wh_f) = 70, 100, 130, \text{ and } 160 \text{ fb}$. The four solid lines correspond to the complementary mechanism $pp \rightarrow H^\pm h_f$ for the same values of the cross section $\sigma(H^\pm h_f)$, and taking $m_{H^\pm} = 150 \text{ GeV}$. As before, the standard mechanism is dominant at low values of $\tan \beta$ and the complementary mechanism dominates at high $\tan \beta$ and this is due to a dependence of the partonic cross section on $\cos^2 \beta$ and $\sin^2 \beta$ respectively. Due to phase space effects, the dependence on $m_{h_f}$ is stronger compared with the LC case, making the equal cross section contours less vertical. For this reason, the depression already observed in the previous figure is less pronounced at the LHC.

In Fig. 6 and 7 we plot contours of constant production cross section at the LC and LHC respectively, in the $m_A - m_{h_f}$ plane for the LC and in the $m_{H^\pm} - m_{h_f}$ plane for the LHC, using the same numerical values for the cross sections as in Figs. 4 and 5. In both cases we take $\tan \beta = 20$, where the standard production mechanisms are very suppressed. If a realistic simulation of the signal were made and the minimum number of events $N_{\text{min}}$ were known for the signal to be observable, the observable cross sections would be of
Figure 7: Curves with constant production cross section $\sigma = 70, 100, 130$, and 160 fb at the LHC in the $m_{h_f} - m_{H^+}$ plane for $\tan \beta = 20$ GeV.
the type $\sigma > N_{\text{min}}/\mathcal{L}$, implying that the region below and to the left of the curves in both figures would be observable. From the figures we see that to increase the region of observability, the minimum cross section needs to be decreased more sharply at the LHC rather than at the LC.

In a similar way, in Figs. 8 and 9 we plot contours of constant production cross section at the LC and LHC respectively, in the $m_A - \tan \beta$ plane for the LC and in the $m_{H^+} - \tan \beta$ plane for the LHC. The chosen values for the cross sections are the same as in the previous figures, and we take a fermiophobic Higgs mass $m_{h_f} = 120$ GeV in both cases. The largest cross sections lie towards the bottom right-hand corner of the figure. The stronger dependence of $\sigma(pp \to H^\pm h_f)$ on $m_{H^+}$ is evident from the figures when compared with the dependence of $\sigma(e^+e^- \to A^0h_f)$ on $m_A$.

In all the situations studied here the directly produced fermiophobic Higgs boson decays into two photons with a branching ratio close to unity if $m_{h_f} < \sim 80$ GeV, close to 0.5 for $m_{h_f} \sim 95$ GeV, and near 0.01 for $m_{h_f} \sim 145$ GeV. In the case of complementary production at the LHC and LC shown in the previous graphs, the number of 4 photon

Figure 8: Curves with constant production cross section $\sigma = 20, 25, 30,$ and 35 fb at a future LC in the $m_A - \tan \beta$ plane for $m_{h_f} = 120$ GeV.
Figure 9: Curves with constant production cross section $\sigma = 70$, 100, 130, and 160 fb at the LHC in the $m_{H^+} - \tan \beta$ plane for $m_{h_t} = 120$ GeV.
events will be maximized for larger $BR(A^0 \rightarrow Zh_f)$ and $BR(H^\pm \rightarrow W^*h_f)$ and lower $m_{h_f}$. Comparing Figs. 3 and 4 we can see that (for $m_A = 150$ GeV) if the model lies below the curve $\sigma(e^+e^- \rightarrow A^0h_f) \approx 30$ fb in the $m_{h_f} - \tan \beta$ plane then the majority of events will be of the four photon type at the LC. Similarly, comparing Figs. 2 and 5 we see that (for $m_{H^+} = 150$ GeV) if the model lies below the curve $\sigma(pp \rightarrow H^\pm h_f) \approx 130$ fb in the $m_{h_f} - \tan \beta$ plane, then a four photon signal would be plentiful at the LHC. Identifying a lepton from the decay of $W^*$ or $Z^*$ would further reduce backgrounds. After applying a realistic photon identification efficiency for 4 photons ($0.8^4 \approx 0.4$) [30] and multiplying by the appropriate BR factors, signal sizes for $\gamma\gamma\gamma\gamma + l^\pm$ in excess of a few fb are possible in a sizeable region of the $m_{h_f} - \tan \beta$ plane.

At the LHC, the main backgrounds for the $\gamma\gamma\gamma\gamma + l^\pm$ are expected to be the irreducible $\gamma\gamma\gamma\gamma + l^\pm$ from genuine photon production, and the reducible 4 jet plus $l^\pm$, where all four jets are misidentified as a photon. MadEvent [43] estimates the irreducible background to be $\sim 10^{-6}$ fb and thus entirely negligible. The 4 jet plus $l^\pm$ was estimated to be $\sim 130,000$ fb, but this fake photon background can be reduced to a negligible size after applying realistic rejection factors of $10^3$ for each jet [30]. Hence we conclude that $\gamma\gamma\gamma\gamma + l^\pm$ is a robust, relatively background free signature at the LHC. A detailed study of detection prospects in all the channels $\gamma\gamma\gamma\gamma$, $\gamma\gammaVV$ and $VVVV$ will be considered in a separate work.

5 Conclusions

We have considered the phenomenology of a fermiophobic Higgs boson ($h_f$) at the Large Hadron Collider (LHC) and a $e^+e^-$ Linear Collider (LC). We showed that the production mechanisms $pp \rightarrow H^\pm h_f, A^0h_f$ and $e^+e^- \rightarrow A^0h_f$ offer promising cross-sections in the region where the conventional mechanisms $pp \rightarrow W^\pm h_f$ and $e^+e^- \rightarrow h_fZ$ are very suppressed. A more complete search strategy at both these colliders would include these complementary production mechanisms. The potentially large branching ratios for $H^\pm \rightarrow h_fW^*$ and $A^0 \rightarrow h_fZ^*$, would lead to double $h_f$ production, with subsequent signatures $\gamma\gamma\gamma\gamma, \gamma\gammaVV$ and $VVVV$, which need experimental simulations. Production cross sections are similar at both machines, but the larger luminosity and smaller backgrounds at the LC would permit precision measurements necessary to determine the exact nature of the observed fermiophobic Higgs boson.

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