The effect of real and virtual photons in the di-lepton channel at the LHC

Elena Accomando,1,2,∗ Juri Fiaschi,1,2,† Francesco Hautmann,2,3,4,‡ Stefano Moretti,1,2,§ and Claire H. Shepherd-Themistocleous1,2,¶

1School of Physics & Astronomy, University of Southampton, Highfield, Southampton SO17 1BJ, UK
2Particle Physics Department, Rutherford Appleton Laboratory, Chilton, Didcot, Oxon OX11 0QX, UK
3Elementaire Deeltjes Fysica, Universiteit Antwerpen, B 2020 Antwerpen, Belgium
4Theoretical Physics Department, University of Oxford, Oxford OX1 3NP, UK

We present a study of di-lepton production at the CERN Large Hadron Collider with a particular focus on the contribution resulting from both real and virtual photons in the initial state. We discuss the region of phase space in which the invariant mass of the lepton pair is of the order of several TeV, where searches for new physics phenomena yielding a di-lepton signature are presently carried out. We study both the yield and associated uncertainties for all possible topologies in photon-induced di-lepton production and compare these with what is expected in the standard Drell-Yan channel, where quark-antiquark pairs are responsible for the production of lepton pairs. We analyse the impact of these QED contributions on the expected Standard Model background and on searches for new physics. In this latter case, we use the production of an extra heavy $Z'$-boson predicted by the Sequential Standard Model (SSM) as a benchmark process.

I. INTRODUCTION

Photon-Initiated (PI) processes in hadron-hadron collisions can be very important at high invariant masses [1], hence, they are relevant to searches for Beyond the Standard Model (BSM) processes. A prominent example is the study of di-lepton final states, $l^+l^-$ (with $l = e, \mu$), which are used in the search for new massive neutral gauge bosons that are present in a variety of BSM scenarios. Currently, limits on their masses are of the order of a few TeV [2, 3]. Alongside the standard Drell-Yan (DY) contribution, mediated by a $s$-channel photon, $Z$ and (potentially) $Z'$ bosons produced from $q\bar{q}$ annihilation, one has also to account for the PI topologies shown in Fig. 1(a). Here, photons are treated as on-shell (i.e., massless) partons residing inside the proton and participating in its internal dynamics governed by both Quantum Chromo-Dynamics (QCD) and Quantum Electro-Dynamics (QED) effects (see for instance Ref. [4]). In this scenario, one has to define a Parton Distribution Function (PDF) for the photon, in the same way as for (anti)quarks and gluons. To accomplish this, different approaches are taken by different groups and different results are obtained, both in the prediction of the central value of the photon PDF and its error, for a given choice of $x$ (the fraction of proton momentum carried by the photon) and $Q^2$ (the factorisation/renormalisation scale).

An analysis of such results for the hadro-production of di-lepton pairs at the current Large Hadron Collider (LHC) was recently presented in [5, 6] (see also Refs. [7, 8]). It was pointed out that the PI contribution can not only be sizeable but even dominant at high invariant masses of the di-lepton pair, which is precisely where $Z'$s are searched for. The PDFs can be affected by very large uncertainties thus generating systematics that can have an impact on data interpretation, at high energy scales. Another possible source of theoretical uncertainty comes from radiative corrections. For the di-lepton final state in particular, these effects have been assessed in Ref. [9].

The PI contribution where the two photons are both real, i.e. massless and on-shell (hence they can be treated as proton constituents), constitutes only one of the possible terms. Terms which allow either one or both photons to be off-shell (i.e. virtual) are also present. This is illustrated in Fig. 1 (see plots (c) and (b), respectively). It is the purpose of this letter to compare the phenomenology of the three mechanisms illustrated to that of DY production of di-lepton pairs in the high invariant mass region.

The layout of the paper is as follows: section II describes the PDF treatment of resolved photons, the EPA approach for low-virtuality photons and the mixed process where one photon is resolved and the other is virtual; section III...
II. PHOTON INDUCED PROCESSES

In this section we discuss the three contributions in Fig. 1 to the di-lepton final state coming from photon induced processes. We start with the inelastic proton-proton scattering giving rise to two resolved photons described by QED PDFs. This term is called double dissociative (DD). Then, we discuss the second term coming from the elastic proton-proton scattering, where the photons are emitted with low virtuality. This contribution is calculated in the Equivalent Photon Approximation and is usually referred to as the EPA term. Finally we evaluate the single dissociative (SD) contribution to the di-lepton spectrum coming from one resolved and one low-virtuality photon.

The contribution to the di-lepton spectrum induced by two incoming real photons can be written as

$$\frac{d\sigma_{DD}}{dM_{\ell\ell}} = \int dx_1 dx_2 \frac{1}{32\pi M_{\ell\ell}} |M(\gamma\gamma \to l^+l^-)|^2 f_\gamma(x_1, Q) f_\gamma(x_2, Q)$$  \hspace{1cm} (II.1)

where the function $f_\gamma(x, Q)$ is the photon PDF, the variables $x_{1,2}$ are the fraction of proton energies taken away by the two photons and $Q$ is the factorisation scale. The observable $M_{\ell\ell}$ is the di-lepton invariant mass. The PDF error is estimated in different ways by different collaborations. NNPDF3.0 provides uncertainty estimates following the “replicas” method [10], while CT14QED follows the Hessian procedure [11], giving a table of 31 PDFs each one associated with a fixed amount of the proton energy fraction carried by the photon. We estimate the error on the Double-Dissociative contribution to the di-lepton production, following the different approaches adopted by the various PDF collaborations (see Ref. [5, 6] for details). The more recent LUXqed set [12] has been delivered in the LHAPDFv6 format [13], and is accompanied by a set of 100 symmetric Hessian eigenvalues to estimate the PDF uncertainties, following the procedure explained in Ref. [14]. The MRST2004QED collaboration does not provide a recipe for estimating an error. Therefore we only show the results for the central value in this case.

The EPA is used in the literature to evaluate the contribution to the di-lepton final state that comes from two initial low-virtuality photons. In the EPA, the photon flux of the proton is estimated by semi-empirical formulae built on the dipole approximation, whose parameters are fitted to the deep-inelastic electron-proton scattering data [15]. The photon induced differential cross section is obtained by multiplying the photon luminosity by the matrix element of the hard photon-photon subprocess and integrating over the phase space (for details see for example Ref. [16]):

$$\frac{d\sigma_{EPA}}{dM_{\ell\ell}} = \frac{dL_{\gamma\gamma}}{dM_{\ell\ell}} f_{\gamma\gamma} = \int_{Q^2_{\min}}^{Q^2_{\max}} dQ^2_1 \int_{Q^2_{\min}}^{Q^2_{\max}} dQ^2_2 \int dx_1 dx_2 \frac{|M(\gamma\gamma \to l^+l^-)|^2}{32\pi M_{\ell\ell}} N(x_1, Q^2_1) N(x_2, Q^2_2)$$  \hspace{1cm} (II.2)

Here, $Q^2_{\min}$ is determined by the kinematics whilst $Q^2_{\max}$ is arbitrary. This is the main source of error [17]. In order to estimate the uncertainty on the EPA predictions, we have spanned the interval $0.5 \text{ GeV}^2 < Q^2_{\max} < 8 \text{ GeV}^2$. Our implementation has been found to agree with that in Ref. [18]. The bulk of the effect comes from photons with low virtuality, while photons with a virtuality $> 2 \text{ GeV}^2$ do not give an appreciable contribution.

Real photons extracted from the QED PDFs of one proton can interact with the low-virtuality photons of the other proton, producing a real-virtual photon hybrid interaction that is referred to as the Single Dissociative (SD) contribution to the di-lepton final state. In order to estimate this term we integrate over one EPA flux and one photon.
III. QED EFFECTS ON THE SM DI-LEPTON SPECTRUM

The double dissociative contribution to the di-lepton spectrum at high energy scales has been recently analysed by different authors \[\text{(5–7)}\] for LHC centre of mass energies of 8 TeV and 13 TeV. The effect of this photon-photon interaction has also been studied for top-antitop pair production \[\text{(19–21)}\] at the LHC and strong similarities with the lepton channel were found. In the literature, the main focus is on the DD term and its uncertainty. There exist many photon PDF sets in the literature: MRST2004QED \[\text{(22)}\], CT14QED \[\text{(23)}\], NNPDF2.3QED \[\text{(24, 25)}\], APFEL-NN2.3QED \[\text{(26)}\], NNPDF3.0QED \[\text{(27)}\], LUXqed \[\text{(12)}\], xFitter epHMDY \[\text{(28)}\].

Some of the PDF sets, such as CT14QED, include the elastic component from quasi-real photons, while in others, such as CT14QED and MRST2004QED, this is subtracted off. Using the approach we have set out in Section II, we are in a position to check the consistency between this subtraction procedure and our calculations. This will be shown in Fig. (d) where we will compare the sum of the three terms obtained with the CT14 set,
FIG. 3: (a) Individual photon-induced contributions to the di-lepton spectrum at the LHC@13TeV, computed with the MRST2004QED PDF set. From bottom to top, we show the contribution from two virtual photons in EPA (black solid line and shaded area), from one real and one virtual photon (SD) (darker coloured line and shaded area), and from two real photons described by QED PDFs (DD) (light coloured line and shaded area). The top black dashed line is the reference DY spectrum. The top-right inset plot shows the ratio between the SD and DD contributions as a function of the di-lepton invariant mass. (b) same as (a) with the CT14QED PDF set. The shaded areas represent the error coming from photon PDFs and/or from the $Q_{\text{max}}^2$ choice in EPA.

with the inclusive result obtained with CT14QED_{inc}, finding a good agreement. In Fig. 4 we will also examine the case of LUXqed, and find that it gives results close to those of CT14QED_{inc} when evaluating the di-lepton spectrum at high scales. The sets NNPDF3.0QED and xFitter_{epHMDY} do not attempt to separately model elastic and inelastic photon components. They perform fits to data inclusively, and this results into much larger uncertainties than CT14 and LUXqed. The NNPDF3.0QED set is the last release of the NNPDF collaboration including photon PDFs. In order to analyse the leptonic pair production at the LHC RunII, in Fig. 2(a) we therefore choose to show the predictions for the photon induced contribution to the di-lepton spectrum coming from the three representative PDF sets MRST2004QED, CT14QED, NNPDF3.0QED.

For the first two PDF sets we show separate results for the DD and the SD term, while for the latter we show the inclusive result, and we compare these contribution to the SM Drell-Yan (DY) spectrum. For each prediction, we include the associated error bands, estimated as discussed above. We apply standard acceptance cuts on rapidity and transverse momentum of the two final state leptons: $|\eta_l| < 2.5$ and $p_T^{l} > 20$ GeV (see Ref. [29]). We find that the three PDF sets agree quite well for the DY channel prediction plus uncertainty. The three curves in fact overlap within the NNPDF3.0 error band, which in the DY case is quite narrow. The effect of the two initial real photons has instead different outcomes. The prediction from CT14QED is by far the smallest one, followed by MRST2004QED. The PI central value given by NNPDF3.0QED is overwhelming the MRST2004QED and CT14QED predictions. The agreement between the various PDF collaborations is not optimal, if we look at the central values. The discrepancy between the fit driven CT14QED and the modelled MRST2004QED is also significantly bigger than the CT14QED error band. However, the NNPDF3.0QED error on the spectrum is so large at high scales that one can conclude that all PDF sets are in good agreement with each other, within that assumed accuracy. The consequence of this assumption is that we are in the presence of a very large theoretical systematics at high scales. For $M_H > 3$ TeV, the theoretical uncertainty on the leptonic DY channel, using the NNPDF3.0QED set, is of the order $O(100\%)$ and more.

In this paper we examine the SD and EPA contributions to the di-lepton spectrum at the LHC to investigate their possible relevance at high invariant masses. Interestingly, the SD term is found to be sizeable and not extremely sensitive to the chosen PDF set. Also the same hierarchy as the DD term when varying PDFs is displayed, but to a much lesser degree, as visible in Fig. 2(b) where we compare the predictions for the SD term given by the two selected PDF sets (the colour code is the same as in Fig. 2(a)). For completeness we also show the effect of different choices of the factorization scale in Fig. 2(c) and Fig. 2(d) respectively for the DD (or the fully inclusive result for the NNPDF3.0QED choice) and the SD terms. The effect of scale variation has also been explored in Ref. [5], where it is visible that for the choice $Q^2 = p_T^2$ as well we do not observe significant deviations. The EPA term is displayed in Fig. 3 and found to be negligible. This figure shows the three photon-induced contributions to the di-lepton spectrum for a centre of mass energy of 13 TeV at the LHC, and we compare them to the DY channel, for the two non-inclusive PDF sets separately. In Fig. 3(a), we show the results obtained by using the MRST2004 set. From bottom to top, we display the contributions to the spectrum that come from two initial low-virtuality photons treated in EPA (black
curve and shaded area), the SD interaction between a real and a low-virtuality photon (deep green curve and shaded area) and the DD interaction between two initial resolved photons. The solid lines give the central value while the shaded areas represent the PDF uncertainty, when available. The black dashed line on top of the plot is the pure DY channel at the QCD and EW lowest order, generated by the quark-antiquark interaction. The EPA term is subdominant compared to the SD and DD contributions. As to these latter ones, the top-right inset plot of Fig. 4(a) shows the ratio between the single and double dissociative central values. The ratio decreases with increasing di-lepton invariant mass. Beyond the 2 TeV region, of interest for BSM searches, the SD contribution is 30 - 40% of the DD one. In this case, the error on the SD term comes only from the treatment of the virtual photon in EPA as the MRST2004 set does not provide any PDF uncertainty.

In Fig. 4(b), we show the same photon induced contributions to the di-lepton spectrum evaluated using the CT14QED set of PDFs. The EPA contribution (black curve and shaded area) is obviously unchanged, as it doesn’t involve PDFs. Following the color code of Fig. 4, we display the SD term (deep blue curve and shaded area) and the DD term (light blue curve and shaded area). The reference DY spectrum is given by the top curve (black dashed line), computed with CTEQ6L. The SD term shows the same behaviour as the DD one, when comparing MRST2004QED with CT14QED. The CT14QED result is in fact slightly smaller than the MRST one over the entire mass range. However, in contrast to the MRST2004 result given in Fig. 4(a), the magnitude of the SD contribution is now of the same order as the DD one. The two contributions overlap within the DD error band. This is explicitly shown in the top-right inset plot. There, one can see that the ratio SD/DD is of the order of 80 - 90% for $M_{ll} > 2$ TeV. Both the magnitude of the ratio of the SD to DD terms and the behaviour of this ratio as a function of the energy scale differ between CT14QED and MRST2004QED. For the first PDF this ratio rises and for the second it falls. These two features are actually due almost entirely to the difference in the DD term that the two collaborations have whereas the two SD predictions almost agree to within the error shown.

In summary, the EPA contribution can safely be neglected since it is generally two orders of magnitude smaller than the DY differential cross section. The SD terms given by the different collaborations are in much better agreement than the DD ones. Moreover, the CT14QED result agrees within errors with MRST2004QED, in contrast to the DD case. Even if the SD central values are very similar, the relative impact of the SD term on the total photon induced process depends strongly on the PDF set that is used, as the DD central values predicted by the different collaborations are quite different. As before, the main conclusion is that the SD term generates an additional error to the already large systematic uncertainty in the high invariant mass region of the di-lepton spectrum.

In order to visualise the overall effect due to initial photon interaction, in Fig. 4(a) we plot the complete photon induced contribution to the di-lepton spectrum obtained by summing up the EPA, SD and DD terms for the MRST2004QED set and we compare it to the default DY differential cross section and to the inclusive PI predictions obtained with the NNPDF3.0QED, CT14QED_inc and LUXqed sets. The complete prediction for the invariant mass distribution of the di-lepton pairs including the overall PDF uncertainties for each PDF set is visible in Fig. 4(b). There is a substantial overlap between the CT14QED_inc and the LUXqed results such that they cannot be disentangled in this plot scale. The prediction of the theoretical errors is quite different in the various PDF set, and some of them are not visible in the previously discussed plot scales. In Fig. 4(c), using the rescaling factors visible in the legend, we show the relative size of the photon PDF error with respect to the complete result, sum of the PI and the DY contributions. The most accurate prediction is given by the LUXqed set, where the photon PDF relative error is always below 0.2% over the entire spectrum. The most conservative scenario is given by the NNPDF3.0QED set, where the photon systematics grow above 10 times the central value in the high invariant mass region. The CT14QED_inc has an error lying between 1% and 4% along the spectrum. If we consider the predictions of the CT14QED_inc or LUXqed, the PI contribution can be safely neglected in BSM searches based on the di-lepton spectrum. In the NNPDF3.0QED case instead, the PI contribution and its uncertainty are statistically relevant already at the ongoing LHC RunII. With the present collected luminosity $\mathcal{L} \simeq 13 fb^{-1}$, one would expect zero SM background events beyond $M_{ll} = 3$ TeV. If taking into account the NNPDF3.0QED uncertainty, one could possibly have up to 3 events at that mass scale. This result could have a profound impact on BSM searches for wide resonances and in particular non-resonant scenarios, like contact interactions, where the SM background is estimated from theory as we discuss in the next section.

As a cross check to exclude possible double counting intrinsic in the QED PDFs definition, we have compared the PI contribution obtained through eq. 11 using the inclusive CT14QED_inc set, with the sum of the three separate terms EPA, SD and DD obtained using the CT14QED set. The result is shown in Fig. 4(d) where we plot the ratio between these two quantities (blue line). Here we can appreciate that using different PDF definitions we are able to separate inclusive and exclusive contributions, keeping the double counting at the level of percent or below. In the same plot we show the comparison between the two close central values for the PI obtained with the LUXqed and the CT14QED_inc sets, their differences being below 7% in all the spectrum.

In the next section we examine implications of the above results on $Z'$-boson searches at the LHC. As noted earlier, the LUXqed set is the set which gives the smallest photon PDF uncertainties, while NNPDF3.0QED gives the largest.
IV. QED EFFECTS ON $Z'$-BOSON SEARCHES

In this section, we will explore the impact of the photon induced processes on searches for $Z'$ resonances in the di-lepton channel for an LHC centre of mass energy of 13 TeV. For a review of $Z'$-boson physics see Refs. [30–33] and references therein.

In this paper we adopt the recently published NNPDF3.0 for computing both the $Z'$-boson signal and the SM background taking into account the photon induced contributions. The earlier paper on this topic in Ref. [5] used the NNPDF2.3 set. While there is no observable change in the $Z'$-boson signal and the SM DY background, both induced by quark-antiquark interactions, the QED terms have been improved. The NNPDF3.0QED set has significantly reduced the global photon induced central value by a factor of 1.7 - 1.8 for $M_{ll} > 3$ TeV. Moreover, it has slightly decreased the error band by roughly 20% in the same invariant mass region, while still preserving the agreement between all PDF collaborations. We use inclusive sets results to examine the consequences of photon-induced contributions to the di-lepton spectrum on $Z'$-boson searches at the LHC. As already shown in Ref. [5], bump searches for narrow resonances are not significantly affected by the systematic uncertainties due to initial photon interactions.
This is because these searches are not extremely sensitive to the background shape. It is in the event of searches for wide resonances or for non-resonant new physics, like contact interactions (CI), that systematic uncertainties can play a role. To illustrate the possible impact of such an uncertainty, we assume that the expected SM background is given by the theoretical prediction. For the CI search, one has to assume the theory prediction, indeed, whilst for a wide resonance it may not be so constrained. In this paper, we take as benchmark theory the Sequential Standard Model (SSM) discussed in Ref. [34] with a reasonably rather wide width.

In Fig. 5, we show the di-lepton spectrum for the SSM with $M_{Z'} = 3$ TeV and $Γ_{Z'}/M_{Z'} = 20\%$, considering both the cross section and reconstructed Forward-Backward Asymmetry ($A_{FB}$) distributions observables, adopting the NNPDF3.0QED set (Fig. 5(a) and (b)) and the LUXqed (Fig. 5(c) and (d)). The latter is representative of the CT14QED inc result as well. In computing the $Z'$-boson signature, we take into account the interference between the new heavy $Z'$-boson and the SM $Z$ and $γ$ as discussed in Refs. [35–37]. As visible in the two upper plots, the effects of the PI contribution and of its error are relevant in the NNPDF3.0QED case. PI events are decreasing our sensitivity to a non-resonant signal. In this specific case, computing the significance of the signal before and after the PI effects and systematics inclusion we would see the significance moving roughly from 3.7 to 2.8. On the other hand in the $A_{FB}$ observable the effect of the systematic uncertainty is reduced as expected (see Refs. [38, 39] and Ref. [5] for the case with the inclusion of photon PDFs). If we follow the LUXqed (or CT14QED inc) result (Fig. 5(c) and (d)) clearly the inclusion of PI processes do not have any effect, thus in this scenario the PI component and its uncertainty can be safely neglected in di-lepton channel analysis. It is worth noting that the high PI central value predicted by the NNPDF collaboration has measurable effects in the $A_{FB}$ observable, especially in the high invariant mass region.

In general, being angularly symmetric, the inclusion of PI processes leads to a reduction of the overall SM predictions for this observable. Comparing Fig. 5(b) and (d), we can see that in the NNPDF scenario the complete result deviates from the pure DY term, while it is well represented by it in the LUXqed scenario in Fig. 5(d), as here the PI central value is negligible with respect to the DY.
V. CONCLUSIONS

Di-lepton final states in the high invariant mass region $M_{ll} \geq 1$ TeV are one of the primary channels for searches for $Z'$ gauge bosons in BSM scenarios and for precision studies of the SM at the LHC. It was pointed out in [5, 6] that in the high-mass region the contribution of photon-induced di-lepton production, and associated photon PDF uncertainties, could distort the di-lepton SM spectrum shape potentially affecting wide-resonance searches. This could have an even greater impact on the Contact Interaction (CI) type of search where one has to predict the SM background form theory. While for a standard narrow $Z'$ search this is not a source of uncertainty, it can become one of the main sources of theoretical systematics for wide $Z'$-bosons and CI searches.

In this letter we have extended the analysis of works [5, 6] by, on one hand, including the contribution of virtual photon processes and, on the other hand, evaluating the impact of recent updates in photon PDF fits. Using as benchmarks the SM di-lepton spectrum and the GSM-SSM wide-resonance scenario, we have found non-negligible contributions from the single-dissociative process. This points to the relevance of improving in the future the theory of PI processes at the LHC for both QED PDFs and elastic processes.

We have presented a new study of the significance of the BSM signal in di-lepton channels by incorporating both real and virtual photon contributions. Our study examines the need for including the theoretical systematics from PI production in the SM background estimate, depending on different scenarios for photon PDFs, and illustrates the role of analysing the reconstructed $A_{FB}$ in addition to the differential cross section.

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