Modelling the Dynamic Line Parameter of 25 kV AC Railway Electric Traction Lines at Earth Cuttings

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Abstract - Modern electric traction lines are mostly of 25 kV 50 Hz or 60 Hz systems. Shunt admittance exists between earth and traction lines are considered to be uniformly distributed all along their length, and are conveniently neglected from calculations & design of the protection schemes. Fault distance locating algorithms are also designed accordingly. Railway tracks in suburban area shall generally be laid on plane surface and be electrified. However, in developing countries, the railway tracks are electrified at non-suburban areas also to a large extent, where tracks are laid through earth cuttings, tunnels, etc. Analysis on historical data collected from a real traction lines network from a non-suburban area where railway tracks are laid through earth cuttings and tunnel revealed that the parasite capacitance between 25 kV 50 Hz AC traction lines and the earth significantly varies with varying topographical features. Data collected and analyses from the experimental setup, and the validation tests conducted thereon on the real traction line system are summarized in this paper.

Key words: AC electric traction, Angle of cutting, Base width of cuttings, Over Head Equipment (OHE), Parasite capacitance, Varying profiles.

I. INTRODUCTION

Traction Electrification System provides electrical power to the trains by means of; Traction Power Supply System, that includes Traction Sub Stations (TSS) located along the railway track at theoretically equal distance; Traction Power Distribution System (also called as Over Head Equipments or OHE) that is fed at single end consists of conventional catenary system; running rails, and various bonds to the ground (earth). Modelling of AC power line of railway traction is done at par with the short length AC power transmission line \([1]\) \([3]\). Impedance \((Z)\) of short length power transmission lines (of length 80 km or lesser, and with voltage 66 kV or below) comprise an inductive reactance \((jX)\) in series with line resistance \((R)\) per unit length as shown in Fig.1.

The traction line parameters per unit length resistance, inductance, and capacitance are \(R_0, L_0\) and \(C_0\), where \(R_0\) is 0.1 to 0.3\(\Omega \)/km, \(L_0\) is 1.4 to 2.4 mH/km and, \(C_0\) is 10 to 14 nF/km \([6]\). The algorithms made for fault distance calculated by the Distance Protection Relay (DPR) in 25 kV AC electric traction line based on the theories \([8]\) \([9]\) \([10]\) of loop impedance of OHE. In all the cases, the impedance angle of OHE is taken as constant; ie \(\angle 70^0\), and the impedance is considered to be uniformly distributed \([2]\). Fault distance indicated by the DPR has a vital role in determining the degree of reliability of electrified railway transportation system. In a study \([10]\) made on the behaviours of a real 25 kV 50 Hz AC electric railway traction lines while earth fault occurred on them, it was revealed that the generalized model (Fig.1) can’t be fit as it is on AC power high voltage traction lines for developing the algorithm for pin pointing the earth fault on it. The topography at the proximity of OHE can significantly influence on the accuracy of the fault distance locating algorithms.

The angle of the earth faults current, however, is determined by the angle of loop impedance of OHE. If it varies; the distance indicate by the DPR shall also vary with a slight margin, may in terms of few hundreds of meters only. But, those erratic data originate by the Distance Protection Relay on the distance of persisting
earth fault on traction power systems shall cause inordinate delay in detecting them, which in turn shall lead to prolonged supply disruption of train traffic at a wide region. Hence, foolproof algorithms developed duly formulating the variations of the shunt admittance between OHE and earth at various topographical conditions is essential for pinpointing the exact position of earth fault on railway electric traction line. It is obvious that the shunt admittance contributed by the parasite capacitance exists between the OHE and earth depends on the height of OHE from rail level, area of the earth cuttings available at the proximity of the OHE, the base width of the earth cuttings, the angle of the cuttings etc.. However, in the available formula [1] the shunt admittance is calculated by presuming the ground below the power line is flat and wide. But the OHE has many unique features, such as, its altitude is as low as 4.58 M from the ground (rail level), and slope profiling (earth cuttings) made through hillocks to lay railway tracks, with slanting height varies from few centimetres to 18 M covers the OHE from three sides. Besides, the earth cuttings may be present within 3 to 5 M radial distances of OHE for a very long stretch. Hence, the data collections from the experiments conducted on model and the validation test conducted on an actual OHE system are adopted as the methodology.

II. EXPERIMENTAL STUDIES

Experimental studies were conducted in two steps,

A. Data collection

Experiments conducted on the similitude model of OHE set up at laboratory (fig.2) for data collection on the parasite capacitance exists between OHE and earth cuttings, for different angles and different base widths of it at the proximity of OHE, keeping the height of OHE and earth cutting controlled. Readings are given in Table 1. Since the standard angles of earth cuttings in railway systems are 30° for ordinary soil, 45° for laterite, 76° for rocks, and 90° for concrete walls in actual, those are highlighted in bold in the tables 1. In all the cases, the slanting height of earth cutting is kept as 7.8 M and height of lower conductor OHE is kept as 5.6 M, as the controlled variables.

Fig.2. Experimentation on similitude of OHE at laboratory at different angles and different base widths.

| Angle of cutting in Degree | Parasite capacitance between OHE and earth at cuttings with base widths, |
|---------------------------|-----------------------------|
|                           | 6.16 M | 6.72 M | 7.28 M | 7.84 M | 8.4 M | 8.96 M | 9.52 M | 10.08 M |
| 10                        | 14.47  | 14.44  | 14.42  | 14.42  | 14.41 | 14.40  | 14.40  | 14.40   |
| 20                        | 14.55  | 14.51  | 14.48  | 14.46  | 14.46 | 14.46  | 14.45  | 14.44   |
| 30                        | 14.63  | 14.59  | 14.55  | 14.53  | 14.51 | 14.50  | 14.48  | 14.46   |
| 40                        | 14.75  | 14.72  | 14.66  | 14.64  | 14.60 | 14.54  | 14.50  | 14.46   |
| 45                        | 14.83  | 14.77  | 14.74  | 14.70  | 14.65 | 14.60  | 14.53  | 14.46   |
| 50                        | 14.92  | 14.85  | 14.81  | 14.75  | 14.69 | 14.64  | 14.56  | 14.47   |
| 60                        | 15.09  | 15.04  | 14.96  | 14.89  | 14.82 | 14.73  | 14.62  | 14.51   |
| 70                        | 15.38  | 15.31  | 15.21  | 15.10  | 14.98 | 14.85  | 14.70  | 14.53   |
| 76                        | 15.56  | 15.45  | 15.34  | 15.23  | 15.10 | 14.95  | 14.76  | 14.55   |
| 80                        | 15.83  | 15.70  | 15.56  | 15.43  | 15.28 | 15.10  | 14.87  | 14.60   |
| 90                        | 16.25  | 16.11  | 15.98  | 15.81  | 15.65 | 15.43  | 15.10  | 14.68   |
B. Validation test

Parasite capacitance exits between the actual OHE and the earth cuttings were measured (fig.3) for verifying the accuracy of data collected from the experimentation.

Fig.3. Validation test on an actual OHE at earth cutting.

III. RESULTS AND ANALYSIS

Figures 4 to 8 are the plots obtained through the regression analysis made on the parasite capacitances of 25 kV AC traction line with the earth at varying profiles of earth cuttings, with the help of an online statistical tool [11]. Y axis represents the parasite capacitance measured, in nano farad / kilo metre (nF/kM), and X axis represents the base width of earth cutting, in metre (M).

Fig 4. Plot on the parasite capacitances of OHE run through at a 30 degree earth cutting, for different widths of it, at controlled height of earth cutting height & OHE

Fig 5. Plot on the parasite capacitances of OHE run through at a 45 degree earth cutting, for different widths of it, at controlled height of earth cutting height & OHE.
In the regression analysis done with the same online statistical tool [11], non-linear equations, viz. quartic, cubic and quadratic with approximate fit to the curves are also generated by the for different angles of cuttings, viz. 30°, 45°, 76° and 90° whose widths varies from 5.6 M to 10.08 M. Keeping the height of cutting, and the height of contact wire of OHE controlled at 7.8 M & 5.6 M respectively. The equations generated are,

Quartic,

\[ Y = aX^4 + bX^3 + cX^2 + dX + k \]  

(1)
Cubic, \[ Y = aX^3 + bX^2 + cX + k \] (2)
Quadratic, \[ Y = ax^2 + bX + k \] (3)

Where \( Y \) is the parasite capacitance in nano-farad per kilometre (nF/kM), \( a, b, c \) & \( d \) are the coefficients of different powers of the independent variable \( X \), and \( k \) is the constant term (Y intercept). \( X \) is the width of earth cutting in metre (M). Equations are shown in tables 2, 3 & 4.

### TABLE 2. Equations generated in Quartic form.

| Angle of cut | Coef. of \( X^4 \) | Coef. of \( X^3 \) | Coef. of \( X^2 \) | Coef. of \( X \) | \( k \) |
|--------------|-------------------|-------------------|-------------------|----------------|-------|
| 30\(^0\)     | -0.0008           | +0.218            | -0.216            | +0.816         | +13.8 |
| 45\(^0\)     | +0.0011           | -0.0391           | +0.506            | -2.881         | -20.9 |
| 76\(^0\)     | +0.001           | -0.039            | +0.536            | -3.235         | +22.9 |
| 90\(^0\)     | -0.0036           | +0.093            | -0.908            | +3.723         | +11.2 |

### TABLE 3. Equations generated in Cubic form

| Angle of cut | Coef. of \( X^3 \) | Coef. of \( X^2 \) | Coef. of \( X \) | \( k \) |
|--------------|-------------------|-------------------|----------------|-------|
| 30\(^0\)     | -0.0024           | +0.0645           | -0.606         | +16.476 |
| 45\(^0\)     | -0.0043           | +0.097            | -0.801         | +17.09  |
| 76\(^0\)     | -0.0032           | +0.0633           | -0.541         | +16.767 |
| 90\(^0\)     | -0.0189           | +0.385            | -2.842         | +23.544 |

### TABLE 4. Quadratic equations generated.

| Angle of cut | Coef. of \( X^2 \) | Coef. of \( X \) | \( k \) |
|--------------|--------------------|----------------|-------|
| 30\(^0\)     | +0.0081            | -0.173         | +15.391 |
| 45\(^0\)     | -0.0044            | -0.022         | +15.137 |
| 76\(^0\)     | -0.0218            | +0.0979        | +15.799 |
| 90\(^0\)     | -0.059             | +0.5699        | +14.99  |

The Akaike Information Criterion (AIC) [4], the Bayesian Information Criterion (BIC) [5], the R\(^2\) (coefficient of determination in regression analysis) and the adjusted R\(^2\) (adj.R\(^2\)) are also calculated for all those equations separately, and shown in tables 5, 6 and 7.

### TABLE 5. AIC, BIC, R\(^2\) and adj. R\(^2\) for Quartic equations for various angles of earth cutting

| Angle of cut | AIC  | BIC  | R\(^2\) | (adj.R\(^2\)) |
|--------------|------|------|---------|---------------|
| 30 deg       | -74.49 | -73.30 | 0.999   | 0.998         |
| 45 deg       | -64.40 | -63.21 | 0.999   | 0.998         |
| 76 deg       | -74.31 | -73.12 | 0.999   | 0.999         |
| 90 deg       | -51.53 | -50.34 | 0.999   | 0.999         |

### TABLE 6. AIC, BIC, R\(^2\) and adj. R\(^2\) for Cubic equations for various angles of earth cutting

| Angle of cut | AIC  | BIC  | R\(^2\) | (adj.R\(^2\)) |
|--------------|------|------|---------|---------------|
| 30 deg       | -70.45 | -69.47 | 0.998   | 0.997         |
| 45 deg       | -61.81 | -60.83 | 0.999   | 0.998         |
| 76 deg       | -67.70 | -66.71 | 0.999   | 0.999         |
| 90 deg       | -44.97 | -43.98 | 0.999   | 0.999         |
TABLE 7. AIC, BIC, R² and adj. R² for Quadratic equations for various angles of earth cutting

| Angle of cut | AIC       | BIC       | R²       | (adj.R²)  |
|--------------|-----------|-----------|----------|-----------|
| 30 deg       | -58.61    | -57.82    | 0.992    | 0.989     |
| 45 deg       | -48.42    | -47.63    | 0.993    | 0.991     |
| 76 deg       | -38.48    | -37.69    | 0.997    | 0.996     |
| 90 deg       | -22.98    | -22.19    | 0.993    | 0.991     |

IV. CONCLUSION

In the regression analysis done on all sets of data for all the different conditions, the coefficient of determination R² and the adjusted R² are found more than 0.9 (which decides the minimum acceptance level of curve fittings) for all the three forms of equations. However, the highest R² is obtained in the quartic equations, which shall give highest accuracy if utilized in creating fault locating algorithm. But the complexity in resolving the higher degree equations may make the software programming costlier in the software controlled numeric fault locating relays. The quadratic equations are also having very high R² value, in the order of 0.99 and above. In the validation test conducted on the actual OHE system at earth cutting with base width 8.4 metre, height 7.9 metre, and angle of cutting 76°, the parasitic capacitance of OHE of length 1234.2 metre was measured as 18.67 nF, which is equivalent to 15.1279 nF/kM. The parasitic capacitance value calculated using the newly formed quadratic equation (3) for the earth cutting with all the measurements similar to the above is,

\[ \text{Parasite capacitance, } C_p = -0.0218 X^2 + 0.0979X + 15.799 = 15.08316 \text{ nF/kM} \]

The variation of calculated value from the value obtained in the validation test is less than 1 %. This much of variation may contribute the error in the fault distance locating algorithm by few metres only. The variation in the accuracy of pin pointing the fault location on OHE within 100 metre range is generally tolerable by electric traction departments of railway organizations. Hence, using of quadratic equations for finding the parasitic capacitance existing between OHE and the earth cuttings is equally recommendable to create algorithms for pin pointing the fault location on OHE.

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