A novel scheme for processing FMCW-ladar data acquired with low sampling rate

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**ABSTRACT**

The frequency-modulated continuous wave (FMCW) ladar is a useful sensor for remote sensing applications and has been widely used in both the military and civilian fields for precise geospatial data acquisition. Typically, the FMCW-ladar signal is collected by use of the heterodyne detection through the dechirping so as to decrease the sampling rate commensurate with the bandwidth. In this manuscript, we proposed a novel scheme for processing the FMCW-ladar signal acquired through the simplified heterodyne detection, and the sampling rate was the same as that in the dechirp detection. Based on the time–frequency relation of the FMCW-ladar signal, two algorithms were proposed to post-process the echo acquired by the simplified heterodyne detection with the sub-Nyquist sampling rate. For the FMCW-ladar echo data acquired by the simplified heterodyne detection with the same sampling rate as in the traditional dechirp detection, the algorithms can achieve the unambiguous range image retaining the range resolution commensurate with the transmitted chirp bandwidth. The effectiveness of the scheme was validated by simulation and real data processing experiments. The capability of the proposed scheme provides an alternative for the FMCW-ladar system without use of the dechirp detection, which can benefit the future FMCW-ladar and microwave photonics radar applications in the remote sensing.

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1. Introduction

The coherent ladar has been used for both the commercial and military applications, including the range measurement, range-resolved velocity and vibration measurement, range imaging, and synthetic aperture ladar imaging (Beck et al. 2005; Gao, Maurice, and H. Rongqing 2012; Klots, Halmos, and Bulot 2013; Hu et al. 2018; Salas 2021). One of the key capabilities required of the coherent ladar system is to provide the fine range resolution with a high signal-to-noise ratio (SNR). From the radar/ladar community, the FMCW-ladar system can provide the large bandwidth and high SNR. In comparison to the pulsed ladar system, FMCW-ladar transmits chirp with long duration and large bandwidth. Besides, the FMCW-ladar benefits from its lower peak power, smaller volume, and lower cost. Thus, the FMCW-ladar system has been widely used in many applications, such as the remote precision range, range imaging, and SAL imaging (Karlsson and Olsson 1999; Barber et al. 2013; Barber and Dahl 2014; Li et al. 2017).

For the high resolution FMCW-ladar system, the bandwidth can be as large as several gigahertz or even several terahertz. According to the Shannon–Nyquist theorem, directly sampling the received echo acquired by the simplified heterodyne detection requires an unreasonable analog-to-digital converter (ADC) rate (Gao and Hui 2012). Thus, the dechirp detection is employed to compress the bandwidth in the optical domain by using a delayed copy of the transmitted chirp signal as the local oscillator (LO) for the coherent detection. Then an ADC with lower sampling rate can convert the analog signal to the discrete samples. The dechirp technique benefits the FMCW-ladar system and is the most common heterodyne detection in the ladar community (Gao, Maurice, and Rongqing 2012; Li et al. 2017). However, in some applications of the FMCW-ladar with dechirp detection, there are some problems that need to be concerned. First, the delay of the LO should be approximately equal to the round-trip delay of the ladar signal in the space (Meta, Hoogeboom, and Ligthart 2007). This limits the flexibility when the ladar works with varying operating distance. When the difference between the real round-trip delay and the LO delay is becoming larger, the beat frequency may be folded (i.e. wrap around in the frequency domain). Then the folded beat frequency may result in a wrong range measurement. Second, in the real measurement situations, the error between the LO delay and the round-trip time is inevitable. Thus, the beat signal comprises two components, one is the desired with lower beat frequency and the other is of higher beat frequency. This results in a bandwidth loss and energy loss. Third, as the echo and reference

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replica signal are acquired by the dechirp detection, the estimation and compensation of the nonlinear phase are troublesome (Meta, Hoogeboom, and Lichthart 2007). Besides, the delay of the LO is typically accomplished by traveling the LO in the fiber delay line. The platform vibration can affect the fiber line and induce phase noises to the LO, which will degenerate the coherence. Thus, extra measures are needed to isolate the vibration from the fiber line in the airborne applications.

In this manuscript, to avoid those shortcomings of the dechirp detection, a novel scheme for FMCW-ladar with simplified heterodyne detection was proposed. In the practical applications of the FMCW-ladar, the range swath delay (i.e. the round-trip delay difference between the nearest target and the farthest target) is usually much shorter than the chirp duration. Then according to the time–frequency relation of the FMCW, the signal instantaneous bandwidth in the receiver is proportional to the swath, which means that the signal instantaneous bandwidth is much smaller than the chirp bandwidth. Thus, by using the sampling rate higher than the instantaneous bandwidth, signal can be acquired without spectrum aliasing in a short interval. While for the signal in the whole chirp duration, the signal is still spectrum aliased. To effectively process the echo acquired by the sub-Nyquist sampling rate, two post-processing methods were proposed in the manuscript. The methods can achieve the unambiguous range imaging result and retain the range resolution commensurate with the transmitted chirp bandwidth. In the proposed scheme, disadvantages of the dechirp detection were avoided and the ADC rate was the same as that in the traditional dechirp detection scheme.

The rest of the manuscript consists of six sections discussing the novel scheme of the FMCW-ladar system and its processing algorithms. Section 2 describes the previous work related to the manuscript. Section 3 focuses on the time frequency relation analysis and provides the rational for the novel scheme. Section 4 proposes the short-time deramping method for post-processing the echo. Section 5 proposes the SPECAN de-aliasing based method. In Section 6, the simulation and real data processing experiments are both performed. The conclusion is given in Section 7.

2. Related work of the FMCW-ladar

In our previous work, we mainly focused on the FMCW-ladar system with both high repetition frequency and wide bandwidth (Mottet and Nicolas 2016; Li, Mo, and Wang et al. 2018), and the developed system is the basis of the proposed novel scheme in the manuscript.

The generation scheme of the FMCW-ladar signal is illustrated in Figure 1. The generator is mainly based on a LiNbO3-1&Q modulator, which consists of a dual-parallel Mach–Zehnder interferometer (MZI) nested inside a third MZI. In the figure, the red line denotes the driving signal travel line and the blue line denotes the bias voltage control.

By properly biased the MZIs, the output of the modulator can be the same as the radio frequency (RF) driving signal while at the optic waveband. Thus, by setting the RF signal to be of the FMCW signal, the FMCW-ladar signal can be generated, and the wavelength is the same as the seed laser, which is denoted by the continuous wave (CW) laser in Figure 1.

For the traditional FMCW-ladar system and our previously developed system, the delay of the modulator output was used as the LO signal. Thus, the dechirp detection was performed in the optical domain. After the optical dechirp detection, the bandwidth of the electronic signal was decreased drastically. Thus, the echo can be sampled by a slow ADC rate. However, the slow ADC rate was achieved at the cost of the optical delay of the same FMCW-ladar

**Figure 1.** The generation of the FMCW-ladar with high repetition and wide bandwidth.
signal and may induce some troublesome problems such as the limits of flexibility and the loss of the effective power.

3. Time–frequency relation of the ladar echo

The time–frequency relation is shown in Figure 2. In the diagrammatic sketch, the abscissa axis is the range time with the round-trip delay of the center target as the origin. The vertical axis is the range frequency with 0 Hz as the origin. The solid oblique lines denote the linear frequency modulation of the nearest target, the center target, and the farthest target, respectively. $B_{\text{chirp}}$ and $T_{\text{chirp}}$ are the bandwidth and the pulse duration of the transmitted signal, respectively. $B_{\text{swath}}$ is the instantaneous bandwidth depending on the $T_{\text{swath}}$.

Based on the time–frequency relation in Figure 2, we have:

$$B_{\text{swath}} = K_r T_{\text{swath}}$$

(1)

where $K_r$ is the chirp rate of the transmitted signal.

As the instantaneous bandwidth is constant during the chirp duration, the echo can be complex sampled by use of the sampling frequency $F_s$ higher than $B_{\text{swath}}$. However, a certain interval of samples is always needed for the signal processing. Thus, in a small time burst, the bandwidth is

$$B_b = K_r T_b + B_{\text{swath}} = K_r (T_b + T_{\text{swath}})$$

(2)

By using the sampling frequency $F_s \geq B_b$, the received echo can be sampled without spectrum aliasing in the burst. However, in the total time duration of the echo, signal is aliased (Oppenheim and Schafer 1999). By taking the center target as the example, the observed time–frequency relation of the sampled echo is shown in Figure 3. For simplicity and without loss of generality, the sampling frequency is one third of the total bandwidth, i.e. $F_s = B_b / 3$. The observed frequency spectrum is aliased. While in each burst (one third of the total duration), signal has no aliasing and corresponds to a frequency folding due to its frequency center in the burst.

Obviously, even the signal is aliased in the total duration, the signal in each short burst can be properly sampled. This provides the feasibility to obtain the unambiguous range imaging result as the echo sampled by use of the Nyquist sampling frequency. In the following, two post-processing methods are proposed. Both methods can achieve the range image

![Figure 2. Time–frequency relation of the echo.](image)

![Figure 3. The observed time–frequency relation of the sampled echo.](image)
without ghost images and retain the range resolution commensurate with the transmitted chirp bandwidth. The short-time deramping-based method is suitable for range imaging in real-time implementation, while the SPECAN de-aliasing-based method is suitable for the SAL imaging.

4. The short-time deramping-based method

First, according to the constraints of sampling rate and distance range, the collected signals are divided into several time slots in the signal cycle, so that there is no spectrum aliasing in the time slots; for different time slots, short-time deramp processing is adopted, so that the targets of different distances correspond to single frequency signals of different frequencies; because different time slots are processed by deramp, the same signal is generated. The target corresponds to the same frequency in different time slots, so all time slots are spliced directly, and the signal of the whole cycle is analyzed in time-frequency, then the imaging result of range direction non aliasing can be obtained, and the imaging resolution is the same as that of the ideal Nyquist sampling condition.

For a point target, the received echo can be written as:

\[
s(t_r) = \text{rect}\left(\frac{t_r - t_0}{T_p}\right) \exp\left(j\pi K_r (t_r - t_0)^2\right) \exp(-j2\pi f_c t_0)
\]

(3)

where \(t_r\) is the range time, \(t_0\) is the round-trip delay, \(f_c\) is the ladar carrier frequency, \(\text{rect}(\cdot)\) is the rectangular window, which is defined as:

\[
\text{rect}(\frac{t_r}{T_p}) = \begin{cases} 1, & -T_p/2 \leq t_r/2 \\ 0, & \text{else} \end{cases}
\]

(4)

As the derivation mainly concerns the phase, the non-essential amplitude terms are ignored in Equation (3).

Since the signal satisfies the Nyquist sampling theorem in a certain time interval, the received echo signal can be divided into several time burst in the range time. The burst duration is:

\[
T_{\text{burst}} = \frac{F_r - K_r T_{\text{swath}}}{K_r}
\]

(5)

Then, the signal in the burst is:

\[
s_i(t_r) = \text{rect}\left[\frac{t_r - (i - 1/2)T_b - t_0}{T_b}\right] \cdot \exp(j\pi K_r (t_r - t_0)^2) \exp(-j2\pi f_c t_0)
\]

(6)

where \(i = 1, 2, \ldots, N\) is the burst index number along the range time. Compared with the total echo duration, the burst length is very short.

For the \(i\)-th burst, we define the reference deramp function as

\[
h_{r,\text{ref}}(t_r) = \exp[-j\pi K_r (t_r - t_{\text{ref}})^2]
\]

(7)

where:

\[
-T_b/2 + (i - N/2 + 1/2)T_b \leq t_r \\
\leq T_b/2 + (i - N/2 + 1/2)T_b
\]

(8)

and \(t_{\text{ref}}\) is the reference time to perform the short-time deramping.

Multiplying Equation (7) to Equation (6) yields:

\[
s_{i,\text{de}}(t_r) = \text{rect}\left[\frac{t_r - (i - 1/2)T_b - t_0}{T_b}\right] \cdot \exp(-j2\pi K_r t_d t_r) \\
\cdot \exp(j\pi K_r (t_0^2 - t_{\text{ref}}^2)) \exp(-j2\pi f_c t_0)
\]

(9)

where \(t_d = t_0 - t_{\text{ref}}\). The term “short-time” means that the burst duration is far smaller than the chirp duration, and the deramping is performed on a burst basis.

In Equation (7), \(t_{\text{ref}}\) is typically set as the range center delay time so as to convert the signal denoted by Equation (9) to the baseband. By combining all the bursts after deramping, we have:

\[
s(t_r) = \sum_{i=1}^{N} \text{rect}\left[\frac{t_r - (i - 1/2)T_b - t_0}{T_b}\right] \exp(-j2\pi K_r t_d t_r) \\
\cdot \exp(j\pi K_r (t_0^2 - t_{\text{ref}}^2)) \exp(-j2\pi f_c t_0)
\]

(10)

From Equation (10), the recomposed signal after deramping is of single frequency and its frequency is \((-K_r t_d)\).

The previous analysis has been focused on the signal component backscattered by a single target located at \(c t_0/2\). For the practical application, we consider a scene in the swath. Then the total bandwidth of the echo is:

\[
B_{\text{total}} = K_r (t_{\text{max}} - t_{\text{min}}) = K_r \frac{2L}{c} = K_r T_{\text{swath}}
\]

(11)

where \(t_{\text{min}}\) and \(t_{\text{max}}\) are the round-trip delays of the nearest target and the farthest target, respectively, \(L\) is the swath in range. According to Equation (3), the signal denoted by Equation (10) is sufficiently sampled and the non-aliasing frequency spectrum can be obtained. Performing the discrete Fourier transform (DFT) to Equation (10) yields:

\[
s(f_r) = \text{sinc}\left[\frac{T_b (f_r + K_r t_d)}{2}\right] \exp(-j2\pi f_c t_0) \\
\cdot \exp(-j2\pi f_r t_d) \exp(-j\pi K_r t_d^2)
\]

(12)

where \(\text{sinc}(x) = \sin(\pi x)/\pi x\) and \(f_c\) is the range frequency. In Equation (12), the \(\text{sinc}(\cdot)\) term represents the compressed range image and the target is compressed to its frequency \(f_r = -K_r t_d\). The first
exponential term in Equation (12) is the delay phase and can be used for the Doppler measurement and Azimuth resolving. The second and the third exponential terms are constant for a particular target, but they depend on the target position.

For the phase preservation of the coherent detection, extra step is needed to compensate the second and the third terms. The signal after FFT has been compressed, and the main energy has been focused on its peak location \( f_r = K_r (t_0 - t_{yf}) \). Thus, similar to the residual video phase compensation in [11], the compensation function can be developed as:

\[
h_{pp}(f_r) = \exp(j\frac{f_r^2}{K_r}) \tag{13}
\]

Multiplying (13) with (12) yields the final range compressed image as:

\[
s(f_r)|_{f_r=K_r t_0} = \text{sinc}[T_p(f_r + K_r t_0)] \exp(-j2\pi f_r t_0) \tag{14}
\]

The range image is compressed in the frequency domain, and its resolution (in distance unit meter) is:

\[
p = \frac{c}{2K_r T_p} = \frac{c}{2B_r} \tag{15}
\]

where \( B_r \) is the bandwidth of the transmitted signal. The resolution is the same as the theoretical one commensurate with the transmitted chirp bandwidth.

In the range compression, each burst can be processed individually and only a small number of samples in each burst. Thus, the method is computational efficient and suitable for parallel or real-time computing implementation. For real-time implementation, the reference deramp functions for all the bursts can be constructed beforehand. Then along with the arriving of the signal samples, each burst can be processed in real-time one by one in the short interval. Finally, only a long-time FFT is needed to achieve the high resolution range compressed image. The computational amount consists of the short-time deramping (\( F_s \times T_{chirp} \) points complex multiplication), the full-time frequency spectrum analysis (\( F_s \times T_{chirp} \) points FFT), and the residual phase compensation (\( F_s \times T_{chirp} \) points complex multiplication). As the \( F_s \) is much smaller than the chirp bandwidth, the total computational amount decreased significantly. Compared to the traditional match filter-based range imaging method, the sampling rate and computational amount are both decreased significantly.

Also, in some applications such as the SAL imaging, the non-aliased frequency spectrum is needed for the fine image formation. In the RDA and the CSA, some steps of the imaging formation are carried out in two-dimensional frequency domain (Jakowitz et al. 1996; Raney et al. 1994; Bamler 1994; Lanari et al. 2001). Thus, reconstructing the non-aliased spectrum is essential for the echo sampled by sub-Nyquist rate. Here, based on the idea of the SPECAN, a method is proposed to de-aliasing the sub-sampled echo. As the non-aliasing spectrum is reconstructed, the windowing can be performed in frequency domain and the range image can be compressed in time domain. The derivation is as follows.

The received signal of the point target located away from the ladar is denoted by Equation (4). And the de-aliasing is achieved through a convolution with a reference function. The reference function is:

\[
s_{\text{ref}}(t_r) = \text{rect}\left(\frac{t_r}{T_p}\right) \exp\left(-j\pi K_{r,\text{ref}} t_r^2\right) \tag{16}
\]

The convolution of Equation (16) with Equation (4) can be expressed as:

\[
s_i(t_r) = s(t_r) \odot s_{\text{ref}}(t_r)
= \int s(\tau) s_{\text{ref}}(t_r - \tau) d\tau
= \exp(-j\pi K_{r,\text{ref}} t_r^2) \int \text{rect}\left(\frac{t_r - \tau}{T_{echo}}\right) \exp(-j2\pi K_{r,\text{ref}} t_r \tau) d\tau
\tag{17}
\]

By letting \( K_{r,\text{ref}} = K_r \), the Equation (17) can be rewritten as:

\[
s_i(t_r) = s(t_r) \odot s_{\text{ref}}(t_r)
= \exp(-j\pi K_r t_r^2) \exp(-j2\pi f_r t_0) \text{sinc}\{\pi B_r t_r\}
\tag{18}
\]

After the convolution, the range compression is accomplished in range time domain. The resolution of the range compressed image is \( c/2B_r \), the same as the traditional coherent ladar system under the Nyquist sampling rate.

As the received ladar data are sampled by ADC, we investigate the implementation of the SPECAN-based de-aliasing in the discrete domain. The output of the convolution in discrete domain is:

\[
s_i(n\Delta t_o) = \sum_{i=M/2}^{i=M/2} s(i\Delta t_i) s_{\text{ref}}(n\Delta t_o - i\Delta t_i) \tag{19}
\]

where \( \Delta t_i \) is the sampling interval of input signal, which is the same as the ADC sampling interval, \( \Delta t_e \) is the effective sampling interval of the output signal,
$M$ is the number of input signal samples, and we have $M = F_r T_p$. To ensure that the output signal spectrum has no aliasing, we have:

$$\Delta t_o \geq 1/B_r$$  \hspace{1cm} (20)

In order to keep a certain over-sampling ratio, we assume $\Delta t_o = 1/(\alpha B_r)$, where $\alpha > 1$. Then Equation (19) can be written as:

$$s_c(n\Delta t_o) = \sum_{i=-M/2}^{i=M/2} s(i\Delta t) s_{ref}(n\Delta t_o - i\Delta t)$$

$$= \exp[-jnK_r(n\Delta t_o)^2] \sum_{i=-M/2}^{i=M/2} \{s(i\Delta t) \exp[-jnK_r(i\Delta t)^2] \exp(-j2\pi n\Delta t_o i)\}$$

$$\times \text{FFT}\{s(i\Delta t) \exp[-jnK_r(i\Delta t)^2]\}$$  \hspace{1cm} (21)

With $n = -N/2, \ldots, N/2 - 1$, where $N = \text{round}(\Delta t_{swath}/\Delta t_o)$ is the output signal sample number, and $\text{round}(\cdot)$ is the nearest integer function. From Equation (21), the last exponential factor has the form of the Fourier transform (FT) kernel. In order to use the Fast FT (FFT) to the signal denoted by Equation (21), we set $\alpha$ to meet the following equation as:

$$\frac{1}{K_r \Delta t_o \Delta t_o} = N'$$  \hspace{1cm} (22)

where $N' = 2^{\text{ceil}(\log_2 N)}$ with $\text{ceil}(\cdot)$ being the nearest integers greater than or equal operator. Then, we can rewrite Equation (21) as follows:

$$s_c(n\Delta t_o) = \exp[-jnK_r(n\Delta t_o)^2] \sum_{i=-M/2}^{i=M/2} \{s(i\Delta t) \exp[-jnK_r(i\Delta t)^2] \exp(-j2\pi n\Delta t_o i)\}$$

$$\times \text{FFT}\{s(i\Delta t) \exp[-jnK_r(i\Delta t)^2]\}$$  \hspace{1cm} (23)

with $n = -N'/2, \ldots, N'/2 - 1$. From Equation (20), Equation (21), and Equation (22), we have that the $N'$ is of the order of $M$. A small number of zero padding of the input signal is required and then the discrete implementation can be performed by a SPECAN processing (involving a chirp multiplication and a subsequent FFT) and an additional phase multiplication.

From Equation (23), the effective sampling rate of the output signal is

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**Figure 4.** Phase and frequency behavior of the sampled chirp. (a) Phase with samples, (b) Frequency with samples.

**Figure 5.** Range compressed image obtained by the traditional match filter. (a) Output of match filter, (b) local zoom in view.
which is sufficient to sample the received echo data. As the spectrum aliasing has been eliminated, the spectrum of signal denoted by Equation (23) can be obtained by performing the FT directly as:

\[ S_c(k\frac{F_s^o}{N'}) = S(k\frac{F_s^o}{N'}) \cdot S_{ref}(k\frac{F_s^o}{N'}) \]  

where \( k = \frac{-N'}{2}, \ldots, \frac{N'}{2} - 1 \), \( S(\cdot) \) is the Fourier transformation of the transmitted signal \( s(t_r) \) and \( S_{ref}(\cdot) \) is the FT of the reference function \( s_{ref}(t_r) \). Both signals are effectively sampled with \( F_s^o \). Then, those processes that are required to be performed in the frequency domain can be carried out directly. Taking the range compression of Equation (25) in frequency domain as an example, we have:

\[ S_{rc}(k\frac{F_s^o}{N'}) = S_c(k\frac{F_s^o}{N'}) \times H_{chirp}(k\frac{F_s^o}{N'}) \cdot S_{ref}^{*}(k\frac{F_s^o}{N'}) \]  

with \( f_r = F_s^o k/N' \) is the frequency in the discrete domain. \( H_{chirp}(k\frac{F_s^o}{N'}) \) is the match filter of the transmitted signal, which is employed to implement the range compression. \( S_{ref}^{*}(\cdot) \) is the conjugated signal of \( S_{ref}(\cdot) \), which is used to compensate the SPECAN-based de-aliasing processing denoted by Equation (17). As the algorithm is developed in the discrete signal domain, we use the discrete variables.

In Equation (26), the window function can be used as the signal are in the frequency domain. Performing the inverse FT to Equation (26) yields the range compressed image without ghosts in the range time domain. As denoted by Equation (17), the compression of the echo is actually a convolution and the phase preservation can be guaranteed (Lanari et al. 2001).

Figure 6. Range compressed image obtained by short-time deramping method. (a) Range image without ghost. (b) Enlarged view of the targets image. (c) The dB scaled range profile after proper interpolation.
6. Experiment and result

In order to validate the proposed methods for processing the FMCW-ladar signal acquired with low sampling rate, both the simulation and real data processing experiment were carried out.

6.1 Simulation and results

We first demonstrate the effectiveness of the proposed algorithm through simulation. In the simulation, the transmitted bandwidth was 1 GHz, chirp duration was 100 μs, and the wavelength of the seed laser was 1550 nm. Three point targets were located 12 km away from the ladar system, and the distances between couples of the adjacent point targets are 30 cm and 60 cm, respectively. The swath was 200 m. In the receiver, the simplified heterodyne detection was used to acquire the echo with the sampling rate of 100 MHz. The complex sampling rate was only 10% of the transmitted signal bandwidth. The received SNR was 10 dB.

For the sampled echo reflected from a single targets examined in isolation, the time–frequency map are shown in Figure 4. It can be observed that the frequency is folded by 10 times.

By employing the traditional match filter in our previous work (Li et al. 2017), the compressed range image was obtained as shown in Figure 5. Nine ghost images can be observed. The ghost images are caused by the spectrum aliasing as the sampling rate is only 10% of the signal bandwidth. Figure 5(b) shows the enlarged view of target image with the highest intensity. Obviously, the three targets cannot be resolved effectively.

By using the two proposed methods, the echo data were properly processed and the results are demonstrated in Figures 6 and 7, respectively.
From Figure 6, the range compressed image is obtained. In Figure 6(a), ghost images are eliminated. Figure 6(b) shows the enlarged view of the targets image. The designed three targets are resolved clearly. After the proper interpolation, the measured distances between the adjacent targets are 30.2 cm and 60.7 cm as in Figure 6(c), respectively. The range resolution can be calculated by the 3-dB range profile of the target in the right edge. The 3-dB resolution is 12.7 cm in Figure 6(d), which is in accord with the theoretic resolution corresponding to the 1 GHz bandwidth.

The processing result by the SPECAN de-aliasing method is shown in Figure 7. From Figure 7, the range compressed image without ghost was also obtained and the three targets were resolved clearly. The measured distances between adjacent targets are 30.6 cm and 59.3 cm, which is in accord with the real setting. From Figure 7(d), the 3-dB resolution of the range profile is 11.9 cm. The range resolution commensurate with the transmitted ladar bandwidth of 1 GHz.

6.2 Real data validation

In order to verify the effectiveness of the proposed methods in the practical situations, a FMCW-ladar system was set up as shown in the Figure 8(a). The modulator is for the generation of the large bandwidth FMCW ladar, which has been discussed in our previous work (Li et al. 2017). The modulated signal was sent to the erbium-doped fiber amplifier (EDFA) for transmitting to the targets. Different from the traditional FMCW-ladar system, the local oscillator (LO) here was of single-frequency from the seed laser. In the receiver, the received echo and the LO were mixed, and the heterodyne signal was obtained. After the balanced photodetectors, echo data were sampled by the analog-to-digital converter (ADC). The modulated signal bandwidth was 10 GHz, the pulse duration was 100 μs, and the ADC rate was 1 GHz. Three corner cubes were located about 75 m away from the ladar system. From Figure 8(b), the relative distances between adjacent cubes are about 7.5 cm and 10 cm.

For the collected real data, the post-processing was performed by employing the proposed algorithms. The reference delay time in Equation (7) was zero in the processing. Figure 8 shows the obtained result. From the figure, the unambiguous compressed range image was obtained and the three cubes can be resolved clearly. The measured distance between the targets and the ladar system is about 75.6 m. In Figure 8(b), the measured relative distances are 7.43 cm and 9.78 cm, respectively. The result is in agreement with the real targets setting in Figure 8(b). The resolution is analyzed in Figure 9(c), and the 3-dB width is about 1.375 cm. For the transmitted ladar signal
with bandwidth of 10 GHz, the theoretic 3-dB resolution is about 1.33 cm. The measured resolution is almost the same as the theoretic one.

7. Conclusion

In conclusion, the manuscript proposed a novel scheme and developed two methods to process the FMCW-ladar data acquired with sub-Nyquist sampling rate. By use of the proposed algorithms, the novel FMCW-ladar system can work effectively without use of the dechirp detection while using the same sampling rate as that in the dechirp detection. Simulation and real data experiment validated the effectiveness of the proposed algorithms. The manuscript provides an alternative scheme for the FMCW-ladar system when the dechirp detection is not suitable. Also, the proposed algorithm benefits the microwave photonic radar for avoiding the dechirp detection.

Disclosure statement

No potential conflict of interest was reported by the author(s).

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Data availability statement

The data that support the findings of this study are available on reasonable request from the corresponding author.

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