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Clustering and halo abundances in early dark energy cosmological models

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ABSTRACT

Cold Dark Matter with cosmological constant (ΛCDM) cosmological models with early dark energy (EDE) have been proposed to resolve tensions between the Hubble constant \( H_0 = 100 h \, \text{km} \, \text{s}^{-1} \, \text{Mpc}^{-1} \) measured locally, giving \( h \approx 0.73 \), and \( H_0 \) deduced from Planck cosmic microwave background (CMB) and other early-Universe measurements plus ΛCDM, giving \( h \approx 0.67 \). EDE models do this by adding a scalar field that temporarily adds dark energy equal to about 10 per cent of the cosmological energy density at the end of the radiation-dominated era at redshift \( z \approx 3500 \). Here, we compare linear and non-linear predictions of a Planck-normalized ΛCDM model including EDE giving \( h = 0.728 \) with those of standard Planck-normalized ΛCDM with \( h = 0.678 \). We find that non-linear evolution reduces the differences between power spectra of fluctuations at low redshifts. As a result, at \( z = 0 \) the halo mass functions on galactic scales are nearly the same, with differences only 1–2 per cent. However, the differences dramatically increase at high redshifts. The EDE model predicts 50 per cent more massive clusters at \( z = 1 \) and twice more galaxy-mass haloes at \( z = 4 \). Even greater increases in abundances of galaxy-mass haloes at higher redshifts may make it easier to reionize the universe with EDE. Predicted galaxy abundances and clustering will soon be tested by the James Webb Space Telescope (JWST) observations. Positions of baryonic acoustic oscillations (BAOs) and correlation functions differ by about 2 per cent between the models – an effect that is not washed out by non-linearities. Both standard ΛCDM and the EDE model studied here agree well with presently available acoustic-scale observations, but the Dark Energy Spectroscopic Instrument and Euclid measurements will provide stringent new tests.

Key words: large-scale structure of Universe – dark matter – galaxies: haloes – methods: numerical.

1 INTRODUCTION

Combined late-universe measurements give the value of the Hubble constant \( h = 0.733 \pm 0.008 \) according to a recent review of Verde, Treu & Riess (2019). This value of the expansion rate is in as much as 6σ conflict with the value \( h = 0.674 \pm 0.005 \) from the Planck measurements of the cosmic microwave background (CMB) temperature and polarization and other early-universe observations extrapolated to the present epoch using standard ΛCDM (Planck Collaboration VI 2018). This discrepancy is unlikely to be a statistical fluke, and it is not easily attributable to any systematic errors (e.g. Freedman 2017; Riess et al. 2019; Aylor et al. 2019). Instead, it may be telling us that there is a missing ingredient in standard ΛCDM. Of the many potential explanations that have been proposed, a brief episode of early dark energy (EDE) around the time of matter dominance followed by ΛCDM evolution (Poulin et al. 2019; Knox & Millea 2020; Smith, Poulin & Amin 2020; Agrawal et al. 2019; Lin et al. 2019) has received perhaps the most attention. For the model we consider here, Poulin et al. (2019) and Smith et al. (2020, SPA20) have shown that their fluctuating scalar field EDE model can fit all the CMB data as well as the usual standard 6-parameter ΛCDM does, and also give \( H_0 \) in agreement with the recent local-universe measurements. As Fig. 1 shows, in this model the EDE contributes a maximum of only about 10 per cent to the total cosmic density at redshifts \( z \approx 3500 \), at the end of the era of radiation domination and the beginning of matter domination.

The resulting best-fitting cosmic parameters (see Table 1) are interestingly different from those of standard ΛCDM. In particular, both the primordial power spectrum amplitude \( A_s \) and \( \sigma_8 \), measuring the linear amplitude today at \( 8 \, h^{-1} \, \text{Mpc} \), are larger than for the latest Planck analysis with standard ΛCDM. Also, \( n_s \), the slope of the
The power primordial power spectrum is larger than for standard $\Lambda$CDM. And with the higher $H_0$, the present age of the universe is 13.0 Gyr rather than 13.8 Gyr. Such modifications of the cosmological parameters are also produced in other recent papers on EDE (Agrawal et al. 2019; Lin et al. 2019; Poulin et al. 2019; Smith et al. 2020) were able to find regions of the parameter space of EDE models that provide a good fit to the data. Still, more work must be done – both in terms of theory and new measurements – to assess the nature of viable EDE models.

We have chosen to focus on the Smith et al. (2020) version of EDE because it was engineered to fit the details of the high-$l$ CMB polarization data, and because it represents the best fit to the local $H_0$ measurements and the largest deviation of the cosmological parameters from standard $\Lambda$CDM, which should lead to the clearest differences in testable predictions. These new cosmological models will make specific predictions for galaxy mass and luminosity functions and galaxy clustering. Given that these phenomena arise from non-linear evolution of primordial perturbations and involve gas dynamics, the power of numerical simulations is essential. Of course, it is possible that the result of such observational tests of EDE will be to eliminate this class of cosmological models. But if not, EDE potentially tells us about a phenomenon that contributes to early cosmic evolution, and about another scalar field important in the early universe besides the putative inflaton responsible for the cosmic inflation that set the stage for the big bang.

The key features that distinguish EDE from LCDM (smaller sound horizon, higher $\Omega_m h^2$, higher $n_s$) are shared by all types of EDE model suggested to resolve the Hubble tension, and even by many other ‘early-universe’ solutions. Unless additional ‘interactions’ are added, the naive requirement of an increase in $H(z)$ at $z \gtrsim 1000$ will necessarily require such shifts in these cosmological parameters to compensate the early integrated Sachs–Wolfe effect in the CMB (Poulin et al. 2019; Hill et al. 2020), as well as keeping the BAO scale fixed at late times (Jedamzik, Pogosian & Zhao 2020). The model we study here is thus a well-motivated proxy for testing a broad category of solutions to the Hubble tension.

There were some earlier efforts to study effects of non-linear evolution in models called EDE (Bartelmann et al. 2006; Francis, Lewis & Linder 2009; Grossi & Springel 2009; Fontanot et al. 2012). However, models for the dark energy used in those papers are very different compared with those discussed in this paper. As a matter of fact, there is little in common – with the exception of the name EDE – between those models and the model we consider here. The equation of state $w$ of dark energy $P = w \rho c^2$ in those papers is $w = -1$ only at $z = 0$ and has significant deviations from $w = -1$ at low redshifts. For example, models used by Grossi & Springel (2009) and Fontanot et al. (2012) had $w = -0.7$ at $z = 1$ and $w = -0.4$ at $z = 5$. This should be compared with $w = -1$ at $z \lesssim 1000$ in our EDE model.

In the sense of dynamics of growth of fluctuations in the matter-dominated era in our EDE model, we are dealing with a vanilla $\Lambda$CDM model with the only modification being the spectrum of fluctuations. Even the spectrum of fluctuations is not much different:

![Figure 1. Densities of different components at different redshifts for EDE (the full curves) and the standard $\Lambda$CDM model (the dashed curves). Oscillating early dark energy density (the blue curve) peaks at $z \sim 3500$ when it contributes $\sim 10$ per cent to the total density. Its contribution quickly decreases after that.](https://example.com/image1.png)
a 2 per cent change in $\sigma_8$ and 0.02 difference in the slope of the spectrum. With these small deviations, one might imagine that the final non-linear statistics (such as power, correlation functions, halo mass functions) would be very similar. But instead we find very significant differences, especially at redshifts $z > 1$.

The $S_8$ tension is the conflict between weak lensing and other local observations that imply a relatively low value of $S_8 = \sigma_8 \sqrt{\Omega_m / 0.3}$ and the higher value of $S_8$ of both the Planck-normalized ΛCDM and the EDE model considered here (Smith et al. 2020). Our EDE model has $\sigma_8 = 0.836$, larger than $\sigma_8 = 0.820$ of our fiducial Planck 2013 MultiDark model or the Planck 2018 value $\sigma_8 = 0.811 \pm 0.006$. But what is determined by CMB observations is $\Omega_m h^2$, and the higher value of $H_0$ with EDE means that the resulting $S_8 = 0.830$ is identical to that from Planck 2018 (Combined value, table 1 of Planck Collaboration VI 2018).

The latest weak lensing measurements of $S_8$ are the Dark Energy Survey year 1 (DES-Y1) cosmic shear results $S_8 = 0.782^{+0.027}_{-0.027}$ (Troxel et al. 2018); the Hyper Suprime-Cam Year 1 (HSC-Y1) cosmic shear power spectra, giving $S_8 = 0.800^{+0.025}_{-0.025}$ (Hikage et al. 2019); and the HSC-Y1 cosmic shear two-point correlation functions, giving $S_8 = 0.804^{+0.026}_{-0.026}$ (Hamana et al. 2020). These measurements are all in less than $2\sigma$ disagreement with $S_8 = 0.830$ from Planck-normalized ΛCDM and our EDE model. Hill et al. (2020) claim that the EDE model considered here, and other EDE models, are in serious tension with large-scale structure measurements. They cite the DES-Y1 result $S_8 = 0.773^{+0.026}_{-0.026}$ obtained by combining weak lensing with galaxy clustering (Abbott et al. 2019), which disagrees by 2.3σ with $S_8 = 0.830$. However, Abbott et al. (2019) allowed the total neutrino mass free to vary, which leads to a somewhat lower DES-inferred $S_8$ than that, $S_8 = 0.792 \pm 0.024$, which arises if $\sum m_\nu = 0.06$ eV is fixed, as the Planck team (Planck Collaboration VI 2018) and we have done. Similarly, the shear-only result was analysed by the SPTPol collaboration with the same convention as ours. They obtained $S_8 = 0.79^{+0.04}_{-0.029}$ (Bianchini et al. 2020), to be compared with $S_8 = 0.782 \pm 0.027$ once the sum of neutrino masses is left free to vary (Troxel et al. 2018). While there is indeed some $S_8$ tension between the DES-Y1 measurements and the prediction of our EDE model, it remains true that the addition of a brief period of EDE resolves the ΛCDM Hubble tension and fits the Planck 2018 CMB observations without exacerbating the $S_8$ tension. This is confirmed from table 7 of Hill et al. (2020), where one can read off that the joint DES-Y1 $\chi^2$ goes from 506.4 for ΛCDM to 507.7 for the EDE cosmology, a marginal degradation given that the joint DES-Y1 data have 457 data points (Abbott et al. 2019). This allows us to conclude that the DES-Y1 result does not exclude the presence of EDE.

This was also demonstrated by Murgia, Abellán & Poulin (2020), where MCMC analyses of the EDE model against KiDS and DES data were performed (see also Chudaykin, Gorbunov & Nedelko 2020) for an analysis based on SPTPol data reaching similar conclusions. Additionally, it was recently suggested that the ‘Effective Field Theory’ analysis of BOSS data excludes the EDE solution due to the additional constraints on the CDM density $\rho_{\text{cdm}}$ it provides (D’Amico et al. 2020; Ivanov et al. 2020). However, Smith et al. (2020) show that the ‘constraint’ comes from a small ($\sim 2\sigma$) tension in the reconstruction of the primordial power spectrum amplitude $A_s$ between BOSS and Planck. Nevertheless, it was also shown that EDE can reach a $H_0$ value as high as 71 km s$^{-1}$ Mpc$^{-1}$ and provide a fit as good as the ΛCDM one. Therefore, further measurements by DES, HSC, and other programs will be important tests for cosmological models as they improve the precision of measurements of $S_8$ and other cosmological parameters.

In this paper, we compare for the first time the predictions for large-scale structure observables between standard ΛCDM and EDE. Through a suite of non-linear simulations, we compute the halo mass function and the BAOs (and correlation functions) at various redshifts. We find significant differences that will allow future observations such as those from ROentgen Survey with an Imaging Telescope Array (eROSITA; Merloni et al. 2012), James Webb Space Telescope (JWST),1 Dark Energy Spectroscopic Instrument (DESI),2 and Euclid space mission3 to critically test such cosmologies.

We use extensive N-body simulations to study the effects of non-linear evolution. As a benchmark, we employ a ΛCDM model with the parameters and spectrum of the MultiDark-Planck simulations (Klypin et al. 2016; Rodríguez-Puebla et al. 2016). Table 1 lists those parameters and Fig. 2 compares linear power spectra. MultiDark-Planck is a well-studied ΛCDM model based on the 2013 Planck cosmological parameters (Planck Collaboration XVI 2014) that has been used in many publications. Sophisticated analyses of galaxy statistics applied to different MultiDark-Planck numerical simulations show that the model reproduces the observed clustering of galaxies in samples such as SDSS and BOSS (e.g. Guo et al. 2015; Kitaura et al. 2016; Rodríguez-Torres et al. 2016). Analyses of this kind – matching selection functions, boundaries of observational sample, light cones, and stellar luminosity functions – are difficult to implement and require high-resolution simulations. We plan to do such simulations in the future for the EDE model considered here, but for now we are interested in learning what differences to expect and what statistics should be promising to distinguish between standard ΛCDM models compared with with EDE ones.

In Section 2, we describe the cosmological simulations used in this paper, and in Section 3 we present and discuss the resulting power spectra. In Section 4, we compare the baryon acoustic oscillations and corresponding correlation functions between ΛCDM and the EDE

1James Webb Space Telescope; https://www.jwst.nasa.gov/.
2Dark Energy Spectroscopic Instrument; https://www.desi.lbl.gov/.
3https://www.Euclid-ec.org/
model. In Section 5, we discuss the changes in halo abundances in EDE out to redshift $z = 4$, and explain the origin of these changes. In Section 6, we discuss halo abundance and clustering at even higher redshifts, including implications for reionization of the universe. Section 7 is a summary and discussion of our results.

2 SIMULATIONS

Most of the results presented in this paper are based on new cosmological $N$-body simulations. The simulations were carried out with the parallel particle-mesh code GLAM (Klypin & Prada 2018). Because the GLAM code is very fast, we have done many realizations of the simulations with the same cosmological and numerical parameters that only differ by the initial random seed. A large number of realizations is quite important because the differences between EDE and $\Lambda$CDM models are not very large. This is especially true on long wavelengths $k \lesssim 0.1 \, h \, \text{Mpc}^{-1}$ where the difference in the power spectra is just $\sim 2$ per cent. So, one needs many realizations to reduce the cosmic variance and see the real differences.

All the GLAM simulations were started at initial redshift $z_{\text{init}} = 100$ or $z_{\text{init}} = 150$ using the Zeldovich approximation. Table 2 presents the numerical parameters of our simulation suite: box size, number of particles, particle mass $m_p$, number of mesh points $N_x^3$, cell size of the density/force mesh $\Delta x$, the number of time-steps $N_{\text{step}}$, and the number of realizations $N_r$.

Table 2. Numerical and cosmological parameters of different simulations. The columns give the simulation identifier, cosmology, the size of the simulated box in $h^{-1}$ Mpc, the number of particles, the mass per simulation particle $m_p$, in units of $h^{-1}$ M$_\odot$, the mesh size $N_x^3$, the comoving gravitational softening length $\Delta x$ in units of $h^{-1}$ Mpc, the number of time-steps $N_{\text{step}}$, initial redshift, and the number of realizations $N_r$. Additional smaller scale simulations are discussed in Section 6.

| Simulation | Cosmology | Box | Particles | $m_p$ | $N_x^3$ | $\Delta x$ | $N_r$ | $z_{\text{init}}$ |
|------------|-----------|-----|-----------|------|--------|-----------|------|------------------|
| EDE$_{0.5}$ | EDE | 500$^3$ | 2000$^3$ | $1.3 \times 10^9$ | 7000$^3$ | 0.071 | 253 | 150 | 5 |
| EDE$_{1}$ | EDE | 1000$^3$ | 2000$^3$ | $1.0 \times 10^{10}$ | 7000$^3$ | 0.143 | 136 | 100 | 16 |
| EDE$_{2}$ | EDE | 2000$^3$ | 2000$^3$ | $8.3 \times 10^{10}$ | 7000$^3$ | 0.285 | 130 | 150 | 6 |
| EDE$_{3}$ | EDE | 2000$^3$ | 2000$^3$ | $8.3 \times 10^{10}$ | 4000$^3$ | 0.500 | 130 | 150 | 210 |
| $\Lambda$CDM$_{0.5}$ | MultiDark | 500$^3$ | 2000$^3$ | $1.3 \times 10^9$ | 7000$^3$ | 0.071 | 253 | 150 | 5 |
| $\Lambda$CDM$_{1}$ | MultiDark | 1000$^3$ | 2000$^3$ | $1.1 \times 10^{10}$ | 7000$^3$ | 0.143 | 136 | 100 | 30 |
| $\Lambda$CDM$_{2}$ | MultiDark | 2000$^3$ | 2000$^3$ | $8.3 \times 10^{10}$ | 7000$^3$ | 0.285 | 130 | 150 | 15 |
| $\Lambda$CDM$_{3}$ | MultiDark | 2000$^3$ | 2000$^3$ | $8.3 \times 10^{10}$ | 4000$^3$ | 0.500 | 130 | 150 | 210 |

Limited force resolution does not allow subhaloes to survive in virialized haloes. This is why we study only distinct haloes (those that are not subhaloes) in this paper.

3 POWER SPECTRA

Fig. 2 shows the $z = 0$ linear power spectra of fluctuations in the EDE and $\Lambda$CDM models. Differences between power spectra of fluctuations are relatively small. On long wavelengths ($k \lesssim 0.1 \, h \, \text{Mpc}^{-1}$), the differences are mostly explained by the normalizations: $\sigma_8(\text{EDE})/\sigma_8(\Lambda\text{CDM})^2 = 1.039$. The differences increase on small scales and become substantial. For example, at $k = 5 \, h \, \text{Mpc}^{-1}$ the amplitude of fluctuations in the EDE model is 17 per cent bigger than in the $\Lambda$CDM model.

The reason for this increase comes from the differences in the slope $n_s$ of the primordial power spectra. At first sight, the difference of 0.02 in the slope seems to be small. However, it results in large differences in amplitude when one compares waves that differ dramatically in wavelength: 15 per cent for waves that differ by a factor of 1000 in wavelength. A more subtle effect is related to the halo mass function, which depends not only on the amplitude of fluctuations but also on the slope of the power spectrum.

The domain of BAOs ($k = 0.07 - 0.3 \, h \, \text{Mpc}^{-1}$) is also different in the models. At first glance, the wiggles that are clearly seen in the top panel of Fig. 2 are the familiar BAOs. They are not, though, they are related to BAOs. If the positions of the BAO peaks were the same, there would not have been wiggles in the ratio of the power spectra. Without the EDE component the position of BAO peaks is mostly defined by $\Omega_b/\Omega_m$ and $\Omega_m h^2$ (Eisenstein & Hu 1998). There is an additional effect in EDE models due to the fact that the EDE changes the dynamics of acoustic waves before the recombination. So, the presence of the wiggles tells us that BAO peaks happen at different wavenumbers: in the EDE models the BAOs are shifted to slightly smaller wavenumbers.

Non-linear evolution modifies the power spectra. Fig. 3 shows results of our simulations at redshift $z = 0$. Results from different box sizes and resolutions nicely match each other in overlapping regions. As the result, we stack together different simulations and extend the range of resolved scales.

As clearly seen in Fig. 3 the non-linear evolution dramatically changes the shape of the power spectrum: at $k \gtrsim 0.5 \, h \, \text{Mpc}^{-1}$ the fluctuations are much larger compared with the linear regime. The bump at $k \sim 1.5 \, h \, \text{Mpc}^{-1}$ corresponds to mass $M = (4\pi/3)\Omega_m\rho_c(l/2)^3 \approx 10^{13} h^{-1} M_\odot$ – scale of large galaxies like...
Clustering and halo abundances in EDE models

4 BARYONIC ACOUSTIC OSCILLATIONS

Fig. 4 displays the linear power spectra for the EDE (the solid line) and two ΛCDM models in the domain of the BAO features. In order to appreciate more clearly their overall P(k) shapes and BAO differences, the two ΛCDM models have been normalized to have the same σ8 = 0.836 as that of EDE. One ΛCDM model is otherwise the MultiDark-Planck one (the dot-solid line). The other ΛCDM model (named ΛCDM_EDE, the dashed line) has the same cosmological parameters as EDE but without the effects of the EDE component.

Compared with ΛCDM, the BAO peaks in the EDE model are systematically shifted. This happens because of a combination of different factors: change of the expansion rate before the recombination, change in the Hubble constant, and in the sound horizon. The sound horizon r_d in the EDE cosmology is smaller compared to the ΛCDM_EDE model (r_d = 143.92 Mpc) despite both cosmologies having the same cosmological parameters, and hence the BAO peaks in the latter are shifted towards larger scales. In the concordance ΛCDM models, the positions of the acoustic peaks are defined by Ω_m h^2 and Ω_b h^2 (see Aubourg et al. 2015). But the propagation of acoustic waves is different in EDE models, as the EDE boosts the Hubble rate around z = 0 and thus these two cosmological parameters no longer define the BAO peak positions.

The relative difference between the BAO wiggles in the three cosmologies is better seen in Fig. 5, where we show the deviations for each linear power spectrum from that without BAO features obtained from the (Eisenstein & Hu 1998) ‘non-wiggle’ P_nw(k) fitting formula. The BAO shifts among the three cosmological models are clearly visible, and systematically shifted towards smaller wavenumbers by 1.8 per cent for EDE and 4.4 per cent for ΛCDM_EDE with respect to the ΛCDM BAO positions. This is expected given their corresponding acoustic sound horizon ratios r_d/ r_d^CDM, where r_d^CDM is the sound horizon of our fiducial cosmology, the ΛCDM model.

The BAO position in the spherically averaged two-point clustering statistics, and hence the acoustic-scale distance measurements obtained from large galaxy redshift surveys, are based on the constraints of the stretch or dilation parameter α defined as

\[ α = \frac{\langle D_A(z)/r_d \rangle}{\langle D_A^0(z)/r_d^0 \rangle}, \]

where D_A(z) = cz(1 + z)^2D_A^2H^2(z) is the dilation distance (Eisenstein et al. 2005), D_A is the angular diameter distance, and H(z) is the Hubble parameter. The stretch parameter α is measured from the best-fitting model to the observed isotropic power spectrum or correlation function on the scale range 0.05 h/Mpc < k < 0.3 h/Mpc (see e.g. Anderson et al. 2014; Ross et al. 2015). The latest and more accurate acoustic-scale distance D_A/r_d measurements, relative to the prediction from Planck TT, TE, EE + lowE + lensing (CMB) in the base-ΛCDM model (i.e. our fiducial MultiDark-Planck13 cosmology, see Table 1) are shown in Fig. 6. The curves in Fig. 6 correspond to the model predictions from EDE (solid), MultiDark-ΛCDM (dashed), and ΛCDM with the same EDE cosmological parameters (dash–dotted). We conclude that EDE and our ΛCDM cosmology models both agree well with the observations.

The effect of EDE clearly shows up at later epochs, having its maximum difference ~ 2 per cent at z = 0 compared to ΛCDM. The upcoming DESI and Euclid experiments with sub-per cent accuracy on the acoustic scale measurements will be able to test models such as the EDE one considered in this work. It is interesting to note that ΛCDM+EDE, despite having the same cosmological parameters as EDE but not the same sound horizon scale, predicts

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4 There is no peak real in the power spectrum at those wavenumbers. The peak at k ≈ 1.5 h Mpc^{-1} in Fig. 3 is due to the fact that we scale the power spectrum by factor k^{54}. However, there is a significant change in the slope of the power spectrum from P(k) ∝ k^{-5.5} in the linear regime to much flatter P(k) ∝ k^{-1.25}.
Figure 4. Linear power spectra, scaled with a factor $k^{7/4}$, for the EDE (the solid line) and $\Lambda$CDM (the dot-solid line) models in the BAO domain. A third $\Lambda$CDM model with the same cosmological parameters as EDE but without the early dark matter component is also shown (the dashed line). All models were normalized to have the same $\sigma_8 = 0.836$ to appreciate clearly the overall shape and acoustic oscillation features differences.

Figure 5. BAO wiggles in the linear power spectrum for the three cosmological models: EDE (the solid line), $\Lambda$CDM (the dashed line), and $\Lambda$CDM$_{EDE}$ (the dot-solid line) with the same cosmological parameters as EDE. The plot shows the deviations of the power spectra from that without baryonic oscillations (Eisenstein & Hu 1998). Compared with $\Lambda$CDM, the BAO peaks in EDE are systematically shifted by 1.8 per cent to smaller wavenumbers, and in the case of $\Lambda$CDM$_{EDE}$ by 4.4 per cent to smaller wavenumbers.

$\alpha$ that differs substantially at all redshifts by about 4 per cent; see Fig. 6).

The acoustic-scale distance measurements up to $z = 1.5$ displayed in Fig. 6 include density-field reconstruction of the BAO feature, which is used to partially reverse the effects of non-linear growth of structure formation (see Anderson et al. 2012; Padmanabhan et al. 2012). The shape of the linear matter power spectrum $P(k)$ is distorted by the non-linear evolution of density fluctuations, redshift distortions, and galaxy bias even at large scales $k < 0.2$ h Mpc$^{-1}$. As mentioned above, the shift parameter $\alpha$ yields the relative position of the acoustic scale in the power spectrum (or two-point correlation function) obtained from the data (or simulations) with respect to the adopted $P(k)$ model.

Here, we study the non-linear shift and damping of acoustic oscillations up to redshift $z = 4$ for dark matter in our ensemble of
Our shift results for the acoustic scale towards larger \( k \), relative to the linear power spectrum, and damping values obtained from our analysis are in good agreement with previous works for ΛCDM (e.g. Crocce & Scoccimarro 2008; Seo et al. 2010; Prada et al. 2016). Fig. 8 demonstrates that the non-linear evolution of the BAO shift (bottom panel) and damping (top panel) for the isotropic dark matter power spectrum in both EDE and ΛCDM cosmologies display small differences, with the BAO features being less affected by the non-linear growth of structure formation. Moreover, Bernal et al. (2020) shows that the ΛCDM-assumed templates used for anisotropic-BAO analyses can be used in EDE models as well.

A summary of our BAO results can also be shown in configuration space. In Fig. 9, we see that the BAO peak in the EDE linear correlation function (right-hand panel) is slightly shifted by \( \sim -2 \) per cent to larger radii compared with the ΛCDM model, as expected from their different values of the sound horizon scale at the drag epoch. The impact of non-linear evolution broadens the BAO peaks but it does not reduce the shift differences between EDE and ΛCDM.

### 5 Halo abundances

To study halo mass functions, we use simulations with 500 \( h^{-1} \) Mpc and 1000 \( h^{-1} \) Mpc boxes and mesh size \( N_{\text{h}} = 7000 \). Simulations with larger 2 \( h^{-1} \) Gpc boxes have lower mass and force resolutions – not sufficient for analysis of galaxy-mass halo abundances.

Haloes in simulations were identified with the SO halofinder BDM (Klypin et al. 2011; Knebe et al. 2011) that uses the virial overdensity definition of Bryan & Norman (1998). The resolution was not sufficient for identifying subhaloes, so only distinct haloes are studied.

Fig. 10 shows the halo mass function at different redshifts. The EDE model predicts more haloes at any redshift, but the difference is very small at \( z = 0 \): a 10 per cent effect for very massive clusters \( M \approx 10^{15} h^{-1} M_{\odot} \) and just 1 per cent for Milky Way mass haloes with \( M = 10^{12} h^{-1} M_{\odot} \). These differences hardly make any impact on predicted statistics of galaxies and clusters with observational uncertainties and theoretical inaccuracies being larger than differences in halo abundances.

The situation is different at larger redshifts: the number of haloes in EDE is substantially larger than in ΛCDM. For example, the EDE model predicts about 50 per cent more massive clusters of mass \( M = (3 - 5) \times 10^{14} h^{-1} M_{\odot} \) at \( z = 1 \). The differences increase even more at larger redshifts. For example, the EDE model predicts almost twice more galaxy-size haloes with \( M > 3 \times 10^{12} h^{-1} M_{\odot} \) at redshift \( z = 4 \). These are interesting predictions that can potentially be tested by comparing with abundances of high redshift \( z \gtrsim 1 \) clusters of galaxies (e.g. Bayliss et al. 2014; Gonzalez et al. 2015; Bocquet et al. 2019), abundances of massive galaxies and black holes at \( z > 4 \) (e.g. Haiman & Loeb 2001; Stefanon et al. 2015; Behroozi & Silk 2018; Carnall et al. 2020), and clustering of high-redshift galaxies (Harkane et al. 2016, 2018; Endsley et al. 2020).

Another consequence of the increased mass function in EDE is earlier collapse times. More haloes in EDE at higher redshifts implies that haloes of a given mass \( M \) form earlier in the EDE model. Because the Universe is denser at those times, so are the haloes. At later times, the accretion of dark matter on to the halo gradually builds the outer halo regions resulting in increasing halo concentration (e.g. Bullock et al. 2001). Thus, denser central regions in EDE models should lead to more concentrated haloes.

At first sight, our results on the halo mass functions are puzzling. Halo mass functions are defined by the amplitude of perturbations \( \sigma(M, z) \). However, the normalization of the perturbations \( \sigma_8 \) is just

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\textsuperscript{7}The broadening and attenuation of the BAO feature is exponential, as adopted in our model given in equation (2), with a scale \( \Sigma_{\text{nl}} \) computed following Crocce & Scoccimarro (2006), Matsubara (2008), i.e. \( \Sigma_{\text{nl}} = \left[ \frac{1}{2 \pi^2} \int P_{\text{lin}}(k) dk \right]^{1/2} \).
Table 3. Mean values of the BAO shift and damping at different redshifts obtained from the best-fitting $\alpha$ and $\Sigma_{nl}$ parameters of the $\sim$200 realizations of EDE$_{2B}$ and $\Lambda$CDM$_{2B}$ real-space power spectra (see Table 2). The damping computed from linear theory $\Sigma_{nl}^{th}$ for each cosmology is also listed for comparison.

| Redshift | $\Lambda$CDM | EDE | $\alpha - 1$ (per cent) | $\Sigma_{nl}$ (Mpc h$^{-1}$) | $\Sigma_{nl}^{th}$ | $\alpha - 1$ (per cent) | $\Sigma_{nl}$ (Mpc h$^{-1}$) | $\Sigma_{nl}^{th}$ |
|----------|--------------|-----|-------------------------|-----------------------------|-------------------|-------------------------|-----------------------------|-------------------|
| 4.079    | 0.061 ± 0.020| 2.089 ± 0.052| 2.101| 0.060 ± 0.019| 2.090 ± 0.055| 2.170 |
| 2.934    | 0.080 ± 0.022| 2.745 ± 0.039| 2.703| 0.078 ± 0.020| 2.787 ± 0.042| 2.791 |
| 1.940    | 0.115 ± 0.024| 3.650 ± 0.032| 3.584| 0.110 ± 0.023| 3.729 ± 0.033| 3.699 |
| 1.799    | 0.123 ± 0.024| 3.823 ± 0.031| 3.756| 0.117 ± 0.023| 3.907 ± 0.032| 3.876 |
| 1.553    | 0.139 ± 0.025| 4.162 ± 0.030| 4.095| 0.132 ± 0.024| 4.255 ± 0.031| 4.224 |
| 1.256    | 0.165 ± 0.027| 4.650 ± 0.029| 4.589| 0.154 ± 0.027| 4.755 ± 0.030| 4.731 |
| 1.021    | 0.182 ± 0.026| 5.095 ± 0.026| 5.063| 0.176 ± 0.029| 5.228 ± 0.030| 5.215 |
| 0.775    | 0.228 ± 0.032| 5.688 ± 0.029| 5.656| 0.205 ± 0.032| 5.813 ± 0.030| 5.820 |
| 0.500    | 0.280 ± 0.036| 6.456 ± 0.030| 6.465| 0.247 ± 0.036| 6.591 ± 0.031| 6.641 |
| 0.244    | 0.345 ± 0.042| 7.306 ± 0.033| 7.377| 0.297 ± 0.042| 7.450 ± 0.034| 7.560 |
| 0.007    | 0.390 ± 0.043| 8.184 ± 0.033| 8.354| 0.352 ± 0.049| 8.343 ± 0.037| 8.536 |

Figure 8. Non-linear evolution of the BAO shift (bottom panel) and damping (top panel) for the isotropic dark matter power spectrum in our EDE$_{2B}$ and $\Lambda$CDM$_{2B}$ simulations. The displayed mean values, and 1σ uncertainties, of $\alpha$ and $\Sigma_{nl}$, and given in Table 6, are estimated from the ensemble of individual shifts and damping parameters measured from fitting each of the power spectra, using equation (2), of the EDE and $\Lambda$CDM GLAM simulations.

Figure 9. Right-hand panel: Linear correlation function of dark matter at $z = 0$ on large scales. We plot the correlation function $\xi(R)$ scaled with $R^2$ to remove the main trend of the correlation function. The correlation function in the EDE model is slightly shifted by $\sim 2$ per cent to larger radii as compared with the $\Lambda$CDM model. Left-hand panel: Non-linear correlation function at $z = 0$. Compared to the linear $\xi(R)$, the BAO peak in the non-linear regime slightly shifts to smaller values and becomes wider with smaller amplitude – effects that are well known and well understood. Non-linear effects do not reduce differences between EDE and $\Lambda$CDM models.

Figure 10. Halo mass function at redshifts $z = 0$–4. The full curves in the bottom panel are for the EDE simulations and the dashed curves are for the $\Lambda$CDM simulations. The smaller box and better resolution simulations EDE$_{0.5}$ and $\Lambda$CDM$_{0.5}$ are used for masses below $M \lesssim 10^{14}$ h$^{-1}$ M$_{\odot}$. They are shown as the red curves in the top panel. Larger box and lower resolution simulations EDE$_{2B}$ and $\Lambda$CDM$_{2B}$ (the black curves in the top panel) are used for massive haloes with $M \gtrsim 2 \times 10^{15}$ h$^{-1}$ M$_{\odot}$. At $z = 0$ halo abundances are very similar for the models: EDE predicts $\sim 10$ per cent more of the most massive clusters $M \approx 10^{15}$ h$^{-1}$ M$_{\odot}$ and 1–2 per cent more of galaxy-size haloes with $M \approx 10^{12}$–$10^{13}$ h$^{-1}$ M$_{\odot}$. The differences in abundances increase substantially with redshift.
of radius $R_8$ corresponding to the average mass $M$ inside a sphere of radius $R_8$: $M = (4\pi/3)\rho_0 R_8^3$. Spherical fluctuations that in the linear approximation exceed a density threshold $\delta_c \approx 1.68$ in the real non-linear regime collapse and form dark matter haloes. The halo mass function

$$\frac{dn}{dM} = f(\sigma) \left[ \frac{\Omega_m \rho_{\text{crit}}}{M^2} \right] \frac{d \ln \sigma}{d \ln M}$$

(3)

can be written in a form that depends mostly on one parameter – the relative height of the density peak $\nu$ defined as

$$\nu = \frac{\delta_c}{\sigma(M,z)}.$$  

(4)

There are different approximations for function $f(\sigma)$. We start with the Press–Schechter approximation because it is easy to see the main factors defining the mass function:

$$\left( \frac{M^2}{\Omega_m \rho_{\text{crit}}} \right) \frac{dn}{dM} = \sqrt{\frac{2}{\pi}} \nu \exp \left( -\frac{\nu^2}{2} \right) \frac{d \ln \sigma}{d \ln M}.$$  

(5)

When $\nu$ is small ($\nu \ll 1$), the Gaussian term is close to unity, and the amplitude of the mass functions is linearly proportional to $\nu$, which, in turn, is inversely proportional to the normalization $\sigma_8$. This explains why the EDE mass function is just $\sim 1$–$2$ per cent larger than in $\Lambda$CDM at small $M$ and at $z = 0$: we are dealing with small $\nu$ peaks of the Gaussian density field. As mass increases, the rms of fluctuations $\sigma(M)$ decreases, and eventually $\nu$ becomes large. In this case the Gaussian term dominates, and we expect a steep decline of $dn/dM$. In this regime the ratio of mass functions is equal to $\approx \exp (\nu^2)$, where $\alpha = (\sigma_{8, \text{EDE}}/\sigma_{8, \Lambda \text{CDM}^3} - 1 \approx 0.02$. For example, for 4$\sigma$ fluctuations $\nu = 4$, we expect $\sim 40$ per cent difference. In other words, for high-$\nu$ peaks a small change in the amplitude of fluctuations produces a very large change in the halo abundance. This is exactly what we see in Fig. 10 at large redshifts.

In practice, we use a better approximation for the halo mass function provided by Despali et al. (2016). We find that the approximation is very accurate at low redshifts with the errors less than $\lesssim 3$ per cent for masses $M_h \approx 10^{11} h^{-1} M_\odot$. However, the errors increase with the redshift, becoming $\sim 12$ per cent at $z = 4$ for the $\Lambda$CDM model. The errors also depend on cosmology: at $z = 4$ the error for the EDE model is $\approx 30$ per cent. While not very accurate, the approximation can be used for qualitative analysis.

We are mostly interested in effects of modification of the amplitude $\sigma_8$ and in changes of the slope of the spectrum $P(k)$. For the base model we use $\Lambda$CDM with $\sigma_8 = 0.820$. We start with increasing the amplitude to the same value $\sigma_8 = 0.836$ as in the EDE model. When doing this, we take the same shape of spectrum as in $\Lambda$CDM and increase the normalization. The dotted curves in Fig. 11 show how the mass function changes due to the increased $\sigma_8$. As expected, the high-$\sigma_8$ model has more haloes and the difference increases with mass and with the redshift. However, the shape of the mass function ratios is too steep compared with the $N$-body simulations. Compare, for example, the $z = 0$ curves in Figs 10 and 11. Also, the magnitude of the effect is much smaller at $z = 4$ compared with what it should be.

Now we also change the slope of the power spectrum from $n_s = 0.965$ to the same value $n_s = 0.985$ as in the EDE model while keeping the same high normalization $\sigma_8$. Because the radius $R_8 = 8 h^{-1}$ Mpc of the top-hat filter in the $\sigma_8$ definition was chosen such that the abundance of massive clusters with $M \approx 10^{15} h^{-1} M_\odot$ should stay approximately constant, keeping the same $\sigma_8$ means that cluster abundance does not change much. At the same time, a steeper slope of $P(k)$ means that the amplitude of fluctuations increases for small haloes. As the result, the full curves for tilted and high-$\sigma_8$ models in Fig. 11 are flatter producing more haloes with small mass.

In Fig. 11, we also mark positions of peaks of given $\nu$ height. As expected, the curves start to go up steeply when haloes become high peaks of the Gaussian field.

In summary, the EDE model predicts quite similar ($1$–$10$ per cent) halo abundance as $\Lambda$CDM at low redshifts, significantly increasing at higher redshifts. Most of the increase is due to the change $\Delta n_s = 0.02$ in the slope of the power spectrum with the increase in $\sigma_8$ playing an additional role. These results are well understood in the framework of the theory of the halo mass function, although the analytical approximation by Despali et al. (2016) fails to reproduce the results accurately with errors up to $\sim 30$ per cent being redshift and model dependent.

### 6 Halo Abundances and Clustering at High Redshifts

Results discussed in the previous section show a remarkable increase with redshift in halo abundances in the EDE model (relative to the $\Lambda$CDM model). Here, we study predictions for even larger redshifts. We focus on two issues: (a) the abundance of small haloes at the epoch of recombination ($z = 6$–$10$) and (b) the clustering of haloes at $z = 4$–$6$ that are plausibly measurable with JWST (Endsley et al. 2020).

We make additional simulations using smaller simulation boxes of $50$ and $250 h^{-1}$ Mpc with $2000^3$ particles and force resolutions of $7$ and $36 h^{-1}$ kpc correspondingly, which is substantially better than in the $\text{EDE}_{0.5}$ and $\text{LCDM}_{0.5}$ simulations. In addition to our EDE and $\Lambda$CDM models, we also run a simulation $\text{LCDM}_{0.5}$ with the same parameters as the $\Lambda$CDM model but with lower amplitude of fluctuations $\sigma_8 = 0.75$ that is motivated by weak-lensing results (e.g.
Hamana et al. 2020). Because of the smaller box size, the improved mass resolution of these simulations ($m_p = 1.3 \times 10^5 h^{-1} M_\odot$ and $m_g = 1.6 \times 10^9 h^{-1} M_\odot$) allows us to study halo abundances and halo clustering for haloes with masses as low as $\sim 10^9-10^{10} h^{-1} M_\odot$.

The abundance and clustering of such low-mass haloes is particularly relevant for understanding reionization. The Universe was re-ionized between $z = 6$ and 10 (e.g. Madau & Dickinson 2014), and it is generally accepted that the observed population of relatively bright star-forming galaxies ($M_{UV} < -17$; $M_g > 10^{10} h^{-1} M_\odot$) cannot provide enough ionizing photons (Paardekooper, Khochfar & Dalla Vecchia 2015; Robertson et al. 2015; Finkelstein et al. 2019). However, fluxes from fainter galaxies may be sufficient (Robertson et al. 2015; Yang et al. 2020). The predicted ionizing flux of UV radiation depends on three factors: efficiency of star formation (especially in low-mass haloes), abundance of haloes of different masses at the epoch of re-ionization, and the escape fraction of photons. Theoretical estimates (Finkelstein et al. 2019; Yang et al. 2020) indicate that about 50–60 per cent of ionizing photons were produced by (but not necessarily escaped from) galaxies hosted in haloes with masses $M_h = 10^{10-12} h^{-1} M_\odot$. These estimates are based on halo abundances in the standard $\Lambda$CDM model. Most of the radiation came from galaxies hosted by haloes with mass $M_h > 10^{11} h^{-1} M_\odot$ (Barkana & Loeb 2001; Finkelstein et al. 2019).

We find that the trend of increasing halo abundance ratios persists during the epoch of re-ionization at redshifts $z = 6-10$. For example, at $z = 7.5$ the EDE model predicts 1.8 times more haloes with masses larger than $M = 10^{10} h^{-1} M_\odot$ compared with $\Lambda$CDM. The difference with $\Lambda$CDM low is even more striking: there are more than 3.7 times more haloes above that mass cut in the EDE compared with the $\Lambda$CDM low model. At $z = 10$, the $\Lambda$CDM low model has 8.3 times fewer haloes with $M > 5 \times 10^9 h^{-1} M_\odot$ compared with the EDE model.

Thus, with other parameters fixed, the EDE model would predict a factor of $\sim 1.5-2$ larger ionizing fluxes compared with the $\Lambda$CDM model. Reducing the fluctuation amplitude to $\sigma_8 = 0.75$ would result in reduction of fluxes by a factor of 3–5 compared with $\Lambda$CDM, which would be problematic.

Clustering of high-redshift galaxies is potentially an interesting way to distinguish different cosmological models. Ground observations with the Hyper Suprime-Cam (HSC) Subaru telescope (e.g. Harikane et al. 2016, 2018) and future measurements of large samples of galaxies at $z = 4-6$ with JWST (Endsley et al. 2020) will bring an opportunity to combine galaxy clustering with abundances as a probe for halo masses and merging rates. Theoretical estimates indicate that the observed galaxies at those redshifts should be hosted by haloes with masses in the range $M = 10^{10-12} h^{-1} M_\odot$ (Harikane et al. 2016, 2018; Endsley et al. 2020).

As we saw earlier, the EDE model predicts stronger dark matter clustering and larger halo abundances at high redshifts compared with the $\Lambda$CDM model. Thus, one would naively expect that haloes—galaxies hosted by those haloes—should also be more clustered. However, our simulations show that this is not the case. Here, we use distinct haloes in the EDE5x and $\Lambda$CDM5x simulations to study clustering of haloes with masses $M = (2-5) \times 10^{11} h^{-1} M_\odot$. Fig. 12 shows the results for haloes at $z = 6$ (top panels) and $z = 4$ (bottom panels). Note that the smallest radius plotted, $R = 1 h^{-1}$ Mpc, is significantly larger than the virial radii of these haloes. Thus, the radii presented in the Figure are well in the domain of the two-halo term and are well resolved by the simulations.

The halo correlation functions at those redshifts and radii are nearly power laws, $\xi(R) \approx (R/R_0)^{\gamma}$, with slopes $\gamma \approx -1.7 - 1.9$, which is similar to the slope of Milky Way mass haloes at $z = 0$. The amplitudes of clustering ($R_0$) at high redshifts are remarkably large. For example, at $z = 6$ and $M > 2.5 \times 10^{11} h^{-1} M_\odot$, the clustering scale is $R_0 = 9.9 h^{-1}$ Mpc for $\Lambda$CDM and $R_0 = 8.8 h^{-1}$ Mpc for the EDE model.

Somewhat unexpectedly, the clustering of haloes in the EDE model is smaller than in $\Lambda$CDM in spite of the fact that the dark matter is more strongly clustered in EDE. The differences depend on redshift and halo mass, but those dependencies are weak. Overall, at the same mass cut, haloes in EDE have correlation functions $\approx 20$–30 per cent smaller. When we select haloes with the same cumulative number density, the differences become even smaller ($\approx 10$ per cent). This suggests that measuring clustering at fixed galaxy number density will not be a strong test of EDE. Instead, other mass-sensitive measures (e.g. satellite kinematics or redshift-space distortions) may be more successful probes at high redshifts.

On theoretical grounds, the correlation function of dark matter haloes $\xi_{\text{halo}}$ can be written as a product of two factors: $\xi_{\text{halo}}(R, M) = b^2 \sigma(M) \xi_{\text{lin}}(R)$, where $\xi_{\text{lin}}(R)$ is the non-linear dark matter correlation function and $b$ is the bias factor (e.g. Sheth & Tormen...
expansion rate that is smaller than local measurements by as much as 2 per cent as a consequence of the small νσ-values. But on smaller scales the linear theory differences become stringently.

Higher resolution simulations will be needed for more detailed comparisons with observations. We leave those to future work.

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DATA AVAILABILITY

Data used in this paper (detailed code description, power spectra and halo catalogs) are available on https://www.skiesanduniverses.org Klypin, Prada, Comparat (2017).

REFERENCES

Abbott T. M. C. et al., 2019, Phys. Rev. D, 100, 023541
Agrawal P., Cyr-Racine F.-Y., Pinner D., Randall L., 2019, preprint (arXiv:1904.01016)
Alam S. et al., 2017, MNRAS, 470, 2617
Anderson L. et al., 2012, MNRAS, 427, 3435
Anderson L. et al., 2014, MNRAS, 441, 24
Angulo R. E., Baugh C. M., Frenk C. S., Lacey C. G., 2008, MNRAS, 383, 755
Angulo R. E., Pontzen A., 2016, MNRAS, 462, L1
Ata M. et al., 2018, MNRAS, 473, 4773
Aubourg É. et al., 2015, Phys. Rev. D, 92, 123516
Aylor K., Joy M., Knox L., Millea M., Raghunathan S., Kimmy Wu W. L., 2019, ApJ, 874, 4
Barkana R., Loeb A., 2001, Phys. Rep., 349, 125
Bartelmann M., Doran M., Wetterich C., 2006, A&A, 454, 27
Baugh C. M. et al., 2019, MNRAS, 483, 4922
Bautista J. E. et al., 2018, ApJ, 863, 110
Bayliss M. B. et al., 2014, ApJ, 794, 12
Behroozi P., Silk J., 2018, MNRAS, 477, 5382
Bernal J. L., Smith T. L., Boddy K. K., Kamionkowski M., 2020, Phys. Rev. D., 102, 123515
Bernal J. L., Verde L., Riess A. G., 2016, J. Cosmol. Astropart. Phys., 2016, 019

The mass function of distinct dark matter haloes (those that are not subhaloes) is very similar to that of standard ΛCDM at z = 0, but the number of haloes in EDE becomes substantially larger at higher redshifts. An analytic analysis shows that the number of haloes increases a lot compared to ΛCDM when they correspond to fluctuations with high amplitude ν, where the Gaussian term in the mass function dominates. The increase in the number of rare cluster-mass haloes at z ≥ 1 is mainly due to the increase in σ8 in the EDE model, while the increase in νσ causes a further increase in the number of galaxy-mass haloes at high redshift.

Our N-body simulations of the non-linear evolution of the EDE model show that its power spectrum and halo mass functions agree within a few per cent with those of standard ΛCDM at redshift z = 0, so the successful predictions of standard ΛCDM at low redshifts apply equally to the EDE cosmology. However, the EDE model predicts earlier formation of dark matter haloes and larger numbers of massive haloes at higher redshifts. This means that haloes of the same mass will tend to have higher concentrations. However, they will not have increased clustering. These predictions will be tested by upcoming observations, with all-sky cluster abundances being measured by the eROSITA X-ray satellite, and the abundance and clustering of high-redshift galaxies to be measured especially by JWST (e.g. Endsley et al. 2020).

7 SUMMARY AND DISCUSSION

There are two main tensions between the standard ΛCDM cosmology and local observations, the Hubble tension and the S8 tension. The EDE model considered here resolves the Hubble tension, which is the Planck-normalized ΛCDM predicts a value of the cosmological expansion rate that is smaller than local measurements by as much as 6σ. Such a large discrepancy is unlikely to be a statistical fluke. And it is probably not due to systematic errors because it is seen in different kinds of measurements, in particular Cepheid-calibrated SNe Ia giving h = 0.674 ± 0.006 (Riess et al. 2019, the SH0ES team) and strong-lens time delays giving h = 0.733 ± 0.018 (Wong et al. 2020, the H0LiCOW team).

As we discussed in the Introduction, this Hubble tension can be resolved by adding a maximum of 10 per cent of dark energy to the energy density of the universe for a brief period around the end of the radiation domination era at redshift z ≈ 3500 (Smith et al. 2020, fig. 1). As we also discussed in the Introduction, this EDE model does not exacerbate the relatively small (≈2σ) S8 tension in standard ΛCDM.

In this paper on the EDE model we have focused on the non-linear effects on halo abundance and clustering, including the BAOs. On large scales, the small differences between the linear power spectra of standard ΛCDM and our EDE model are mostly due to the different σ8 values. But on smaller scales the linear theory differences become larger because of the slightly larger slope n8 of the EDE primordial power spectrum. Similar effects are expected in other EDE models that are motivated by resolving the Hubble tension (e.g. Agrawal et al. 2019; Lin et al. 2019).

In this paper, we have explored the non-linear implications of the Smith et al. (2020) EDE model using a large suite of cosmological N-body simulations. When non-linear effects are taken into account, standard ΛCDM and EDE differ by only about 1-10 per cent in the strongly non-linear regime k ≥ 1 h Mpc−1 at low redshift. On the larger scales of the BAOs, in linear theory the peaks are shifted to smaller wavenumbers by about 2 per cent as a consequence of the different value of the sound horizon scale at the drag epoch. Non-linear effects broaden and damp the BAO peaks, but the ≈2 per cent shift to larger physical scales is robust. As Fig. 6 shows, both standard ΛCDM and the EDE model are in good agreement with all the presently available acoustic-scale distance measurements. DESI and Euclid measurements will soon be able to test such predictions more stringently.

The mass function of distinct dark matter haloes (those that are not subhaloes) is very similar to that of standard ΛCDM at z = 0, but the number of haloes in EDE becomes substantially larger at higher redshifts. An analytic analysis shows that the number of haloes increases a lot compared to ΛCDM when they correspond to fluctuations with high amplitude ν, where the Gaussian term in the mass function dominates. The increase in the number of rare cluster-mass haloes at z ≥ 1 is mainly due to the increase in σ8 in the EDE model, while the increase in νσ causes a further increase in the number of galaxy-mass haloes at high redshift.
APPENDIX A: COMPARISON OF GLAM RESULTS WITH THOSE OF DIFFERENT SIMULATIONS AND CODES

The GLAM code has already been extensively tested and compared with other high-resolution simulations in Klypin & Prada (2018). In particular, fig. 2 in Klypin & Prada (2018) presents detailed comparison of power spectra of GLAM simulations with those of the MultiDark simulations (Klypin et al. 2016) that were performed with the GADGET code (Springel 2005). In Hernández-Aguayo et al. (2021), we compare halo mass functions and correlation functions of GLAM and the Planck Millennium simulation (Baugh et al. 2019) again made with the GADGET code. Here, we present more tests.

We start with comparing our results on the power spectrum with the power spectra of the QUIJOTE simulations (Villaescusa-Navarro et al. 2020). The latter used cosmological parameters $\Omega_m = 0.3173$, $\Omega_b = 0.049$, $n_s = 0.9624$, $\sigma_8 = 0.834$, and $h = 0.671$. The simulations were done for $512^3$ particles moving in the computational box $1 \ h^{-1} \ Gpc$. In total there were 15 000 realizations. We use the same cosmological parameters as the QUIJOTE simulations in our GLAM runs. We make two sets of simulations. One set has large box size of $2 \ h^{-1} \ Gpc$ and relatively low resolution of $1 \ h^{-1} \ Mpc$. It is designed to study the accuracy of the code at very long waves. The other set of simulations has smaller box of $1 \ h^{-1} \ Gpc$ and much better force resolution of $0.167 \ h^{-1} \ Mpc$. It is to study small scales. In total we produced 90 new realizations.

To reduce effects of cosmic variance, we make simulations in pairs. In each pair phases of fluctuations are rotated by $180^\circ$. This is done by making one ‘normal’ random realization. For second realization of the pair we change the sign of initial perturbations of the gravitational potential. This dramatically reduces the cosmic
Clustering and halo abundances in EDE models

Figure A1. Comparison of power spectra of QUIJOTE and GLAM simulations at $z = 0$. The top panel shows power spectra for a wide range of wavenumbers. Note that $P(k)$ for Quijote simulations stops declining at $k \sim 3 \, h^{-1}\text{Mpc}$ due to uncertain aliasing and shot noise corrections. The true spectrum must decline at those wavenumbers. The bottom panel focuses on the BAO domain and shows relative errors.

Fig. A1 presents power spectra of QUIJOTE and GLAM simulations. Because of small cosmic variance in $2 \, h^{-1}\text{Gpc}$ GLAM and QUIJOTE simulations, relative errors are less than $\sim 0.3\%$ at $k < 0.2 \, h^{-1}\text{Mpc}^{-1}$. GLAM simulations with $1 \, h^{-1}\text{Gpc}$ boxes have errors less than $\sim 0.5\%$ for $k = (0.3 - 1.5) \, h^{-1}\text{Mpc}^{-1}$. Steep decline of curves at $k > 0.3 \, h^{-1}\text{Mpc}^{-1}$ for $2 \, h^{-1}\text{Gpc}$ simulations and at $k > 2 \, h^{-1}\text{Mpc}^{-1}$ are due to limited force resolutions in GLAM simulations.

The wavenumber $k_{1\,\text{per\,cent}}$ at which the GLAM power spectra fall 1 per cent below the QUIOTE simulations scales linearly with the force resolution $\Delta x = Box/N_g$. We can combine results for the QUIOTE simulations with those presented by Klypin & Prada (2018; fig. 2) for the MultiDark simulations to find dependence of $k_{1\,\text{per\,cent}}$ on the force resolution: $k_{1\,\text{per\,cent}} = (0.25 \pm 0.05)/\Delta x$, where $\Delta x$ is in units $h^{-1}\text{Mpc}$. If we apply this estimate to EDE0.5 and $\Lambda CDM0.5$ simulations for which $\Delta x = 71 \, h^{-1}\text{kpc}$, we find that GLAM power spectra have errors less than 1 per cent for $k < 3.5 \, h^{-1}\text{Mpc}^{-1}$.

In order to test the accuracy of the halo mass function, we compare results of GLAM simulations with those of the 2.1 trillion particles high-resolution simulation Uchuu (Ishiyama et al. 2020), which was done using a $2 \, h^{-1}\text{Gpc}$ box size with massively parallel TREEPM code GREEM (Ishiyama et al. 2015). We use the same cosmological parameters and the same halo definition (spherical ‘virial’ overdensity) as in Uchuu. Parameters of these GLAM simulations are the same as for EDE 1 simulations: $1 \, h^{-1}\text{Gpc}$ box, 8 billion particles, 70003 mesh (force resolution 143 $h^{-1}\text{kpc}$). We made 15 realizations to reduce effects of the cosmic variance.

Fig. A2 presents results of (distinct) halo mass functions at $z = 0$ and $z = 2$. Halo mass function of GLAM simulations become accurate (errors less than 5 per cent) for masses $M > 5 \times 10^{12} \, h^{-1}\text{M}_\odot$ corresponding to haloes resolved with 2.5–3 resolution elements $\Delta x$ along the virial radius.

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