A Simple yet Effective Method for Sentence Ordering

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Abstract

Sentence ordering is the task of arranging a given bag of sentences so as to maximise the coherence of the overall text. In this work, we propose a simple yet effective training method that improves the capacity of models to capture overall text coherence based on training over pairs of sentences/segments. Experimental results show the superiority of our proposed method in in- and cross-domain settings. The utility of our method is also verified over a multi-document summarisation task.

1 Introduction and Background

Document coherence understanding plays an important role in natural language understanding, where a coherent document is connected by rhetorical relations, such as contrast, elaboration, narration, and justification, allowing us to communicate cooperatively in understanding one another. In this work, we measure the ability of models to capture document coherence in the strictest setting: sentence ordering (Barzilay and Lapata, 2005; Elsner et al., 2007; Barzilay and Lapata, 2008; Prabhumoye et al., 2020), a task of ordering an unordered bag of sentences from a document, aiming to maximise document coherence.

The task of sentence ordering is to restore the original order for a given bag of sentences, based on the coherence of the resulting document. The ability of a model to reconstruct the original sentence order is a demonstration of its capacity to capture document coherence. Figure 1 presents such an example, where the (shuffled) sentences are from a paper abstract discussing the relationship between word informativeness and pitch prominence, and the gold-standard sentence ordering is (4, 5, 1, 7, 3, 2, 6). Furthermore, the task of sentence ordering is potentially beneficial for downstream tasks such as multi-document summarisation (Nallapati et al., 2017), storytelling (Fan et al., 2019; Hu et al., 2020), cooking recipe generation (Chandu et al., 2019), and essay scoring (Tay et al., 2018; Li et al., 2018), where document coherence plays an important role.

Traditional approaches to sentence ordering used hand-engineered features to capture document coherence (Barzilay and Lapata, 2005; Elsner et al., 2007; Barzilay and Lapata, 2008; Elsner and Charniak, 2011; Mesgar and Strube, 2016), e.g. using an entity matrix (Barzilay and Lapata, 2005, 2008) or graph (Guinaudeau and Strube, 2013) to represent entity transitions across sentences, and maximising transition probabilities between adjacent sentences.

Neural work has modelled the task either generatively (Li and Hovy, 2014; Li and Jurafsky, 2017; Gong et al., 2016; Logeswaran et al., 2018; Cui et al., 2018; Wang and Wan, 2019; Oh et al., 2019; Cui et al., 2020; Yin et al., 2020; Kumar et al., 2020) or discriminatively (Chen et al., 2016; Prabhumoye et al., 2020). As example genera-
tive approaches, Cui et al. (2020) obtain sentence and paragraph representations from BERT (Devlin et al., 2019) and then use a pointer network to decode the sentence ordering for a given paragraph, whereas Yin et al. (2019) use a graph-based neural network over sentences and entities. The shortcoming of generative methods is the difficulty in obtaining good paragraph representations, especially for longer paragraphs. To mitigate this, various attention mechanisms have been explored (Cui et al., 2018; Wang and Wan, 2019; Kumar et al., 2020).

Discriminative approaches, on the other hand, can readily capture the relative order between sentence pairs, and paragraph decoding can then be achieved through methods such as beam-search (Chen et al., 2016) or topological sort (Tarjan, 1976; Prabhhumoye et al., 2020). However, even with exact decoding methods such as topological sort, issues remain, including: (1) coherence scores for sentence pairs that are distant in the document tend to be noisy; and (2) it can be difficult to determine the relative order of adjacent sentences without broader context. To mitigate these two drawbacks, we propose a simple yet effective training method. Instance pairs are only constructed from adjacent segments to provide stronger coherence signals, but to capture broader context, up to 3 continuous sentences are combined to form a single segment in an instance pair. The effectiveness of our method is demonstrated across multiple datasets, in in- and cross-domain settings, and the setting of multi-document summarisation.

2 Methodology

The method proposed by Prabhhumoye et al. (2020) exploits the relative order between any two sentences in a given paragraph. As in Figure 2a, the pairs connected by blue and red lines (pointing right and left, resp.) are the resulting positive and negative coherence instances for sentence \( s_2 \), respectively. These instances are used to train a text coherence model, which we denote as “allpairs”.

In contrast, our method utilises the relative order between adjacent segments only, resulting in an order of magnitude less training data than allpairs (\( O(n) \) vs. \( O(n^2) \)) but stronger supervision signal; we denote this as “adjonly”. As in Figure 2b, the blue/red lines connect adjacent sentences for sentence \( s_2 \), resulting in positive/negative coherence instances. To capture broader context, we also construct pairs based on segments made up of multiple continuous sentences (not shown in the figure), such as \( (s_1;2, s_2;3) \) and \( (s_1;3, s_2;4) \) as positive instances, and \( (s_2;3, s_1;2) \) and \( (s_2;4, s_1;3) \) as negative instances, where \( s_{i:i+j} \) denotes the concatenation of sentences \( s_i \) to \( s_{i+j} \) inclusive (\( j \geq 0 \)). In this work, we experiment with \( j \in \{0, 1, 2\} \) (i.e. sentence unigrams, bigrams, and trigrams), resulting in (at most) \( 6(n-2) \) instances for a paragraph with \( n \) sentences (noting that the segment cannot extend beyond the extremities of the document).

At test time, following Prabhhumoye et al. (2020), we predict the relative order of each sentence pair (only sentence unigram), then order the sentences with topological sort.

We also trialled other training methods — including regressing over the distance between two sentences, and training with constraints over sentence triplets inspired from Xu et al. (2019a) in computer vision — but observed no improvement.

3 Experiments

3.1 Datasets

We perform experiments over six publicly available datasets from Logeswaran et al. (2018) and Xu et al. (2019b), resp.:

- **NeurIPS, ACL, and NSF**: abstracts from NeurIPS papers, ACL papers, and NSF grants (ave. sentences = 6.2, 5.0, and 8.9, resp.).
- **Athlete, Artist, and Institution**: paragraphs with >10 sentences from Wikipedia articles of athletes, artists, and educational institutions (ave. sentences \( \approx 12 \)).

3.2 Evaluation Metrics

Following previous work, we use 4 evaluation metrics (higher is better in each case):

![Illustration of the baseline method of Prabhhumoye et al. (2020) (a) and our proposed training method (b), where blue and red lines indicate positive and negative segment pairs, respectively.](image-url)
• **Perfect Match Ratio (PMR):** % of paragraphs for which the entire sequence is correct (Chen et al., 2016).
• **Accuracy (Acc):** % of sentences whose absolute positions are correct (Logeswaran et al., 2018).
• **Longest Common Subsequence (LCS):** % overlap in the longest common subsequence between the predicted and correct orders (Gong et al., 2016).
• **Kendall’s Tau (τ):** rank-based correlation between the predicted and correct order (Lapata, 2006).

### 3.3 Model Configuration

We benchmark against Prabhumoye et al. (2020), using a range of text encoders, each of which is trained separately over allpairs and adjonly data.

**LSTM:** each segment is fed into a separate biLSTM (Hochreiter and Schmidhuber, 1997) with the same architecture and shared word embeddings to obtain representations, and the segment representations are concatenated together to feed into a linear layer and softmax layer. We use 300d pre-trained GloVe word embeddings (Pennington et al., 2014) with updating, LSTM cell size of 128, and train with a mini-batch size of 128 for 10 epochs (with early stopping) and learning rate of 1e-3.

**BERT:** predict the relative order from the “CLS” token using pre-trained BERT (Devlin et al., 2019), or alternatively ALBERT (Lan et al., 2020) (due to its specific focus on document coherence) or SciBERT (Beltagy et al., 2019) (due to the domain fit with the datasets). For BERT and ALBERT, we use the base uncased version, and finetune for 2 epochs in each case with a learning rate of {5e-5, 5e-6}.

**BERTSON (Cui et al., 2020):** the current SOTA for sentence ordering, in the form of a BERT-based generative model which feeds representations of each sentence (given the context of the full document) into a self-attention based paragraph encoder to obtain the document representation, which is used to initialise the initial state of an LSTM-based pointer network. During decoding, a deep relational module is integrated with the pointer network, to predict the relative order of a pair of sentences.²

### 3.4 In-domain Results

Table 1 presents the results over the academic abstract datasets. The adjacency-only method performs better than the all-pairs method for all encoders over all evaluation metrics, underlining the effectiveness of our proposed training method. Comparing sentence encoders, the pretrained language models outperform LSTM, with ALBERT and SciBERT generally outperforming BERT by a small margin, demonstrating the importance of explicit document coherence training (ALBERT) and domain knowledge (SciBERT). Overall, SciBERT-adjonly achieves the best over NeurIPS and ACL, and ALBERT-adjonly achieves the best over NSF.

As BERTSON is trained on BERT base, the fairest comparison is with BERT-adjonly. Over NeurIPS, BERTSON has a clear advantage, whereas the two models are perform almost identically over ACL, and BERT-adjonly has a clear advantage over NSF. Note that this correlates with an increase in average sentence length (NSF > ACL > NeurIPS), suggesting that our method is better over longer documents.

Looking to the results over the Wikipedia datasets in Table 2, once again the adjacency-only model is consistently better than the all-pairs method. Here, ALBERT-adjonly is the best of BERT-based models (noting SciBERT has no domain advantage in this case), and despite the documents being longer again than NSF on average, there is remarkable consistency with the results in Table 1 in terms of the evaluation metrics which are explicitly normalised for document length (LCS and τ).

### 3.5 Cross-domain Results

To examine the robustness of our method in a cross-domain setting, we focus exclusively on ALBERT, given its overall superiority in an in-domain setting. We finetune ALBERT over the Athlete dataset, and test over the Artist, Institution, and NeurIPS datasets, resulting in different degrees of topic and domain shift: Athlete → Artist (similar

¹Note that the code for BERTSON has not been released, and given the complexity of the model, we were not confident of our ability to faithfully reproduce the model. As such, we only report on results from the paper, for those datasets it was evaluated over. Similar to Prabhumoye et al. (2020), all sentence pairs are used to learn the sentence representations, aiming to capture the pairwise relationship between sentences.

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| Models             | NeurIPS PMR | NeurIPS Acc | NeurIPS LCS | NSF PMR | NSF Acc | NSF LCS | τ |
|-------------------|-------------|-------------|-------------|--------|--------|--------|---|
| BERTSON           | 48.01       | 73.87       | —           | 59.79  | 78.03  | —      | 0.85|
| LSTM-allpairs     | 14.18       | 43.62       | 71.58       | 26.76  | 50.19  | 75.05  | 0.66|
| LSTM-adjonly      | 18.16       | 47.10       | 74.44       | 30.66  | 53.08  | 76.94  | 0.70|
| BERT-allpairs     | 33.83       | 61.91       | 83.10       | 50.34  | 69.35  | 85.94  | 0.83|
| BERT-adjonly      | 42.29       | 68.06       | 86.23       | 59.79  | 75.96  | 89.72  | 0.86|
| ALBERT-allpairs   | 37.31       | 65.12       | 85.00       | 54.01  | 71.71  | 87.36  | 0.85|
| ALBERT-adjonly    | 41.79       | 68.95       | 86.23       | 60.97  | 76.40  | 90.09  | 0.87|
| SciBERT-allpairs  | 37.31       | 65.55       | 84.65       | 54.74  | 72.23  | 87.40  | 0.85|
| SciBERT-adjonly   | 44.53       | 71.00       | 87.74       | 63.04  | 78.98  | 90.87  | 0.89|

Table 1: Results over the academic abstract datasets (results for BERTSON are those reported in Cui et al. (2020); “—” indicates the number was not reported in the original paper).

| Models             | Athlete PMR  | Athlete Acc  | Athlete LCS | Institution PMR | Institution Acc | Institution LCS | τ |
|-------------------|--------------|--------------|-------------|-----------------|-----------------|-----------------|---|
| LSTM-allpairs     | 0.00         | 15.31        | 49.32       | 0.00            | 12.62           | 46.23           | 0.28|
| LSTM-adjonly      | 0.89         | 30.54        | 64.91       | 0.00            | 24.32           | 60.24           | 0.51|
| BERT-allpairs     | 2.53         | 32.81        | 68.24       | 0.66            | 24.45           | 61.16           | 0.50|
| BERT-adjonly      | 10.17        | 50.52        | 79.56       | 6.93            | 46.59           | 76.82           | 0.76|
| ALBERT-allpairs   | 2.78         | 35.03        | 69.99       | 1.23            | 29.57           | 66.25           | 0.59|
| ALBERT-adjonly    | 14.89        | 56.25        | 82.59       | 9.31            | 49.66           | 79.64           | 0.78|
| SciBERT-allpairs  | 1.14         | 27.97        | 64.47       | 0.38            | 22.36           | 59.72           | 0.47|
| SciBERT-adjonly   | 6.08         | 45.40        | 76.27       | 2.18            | 39.42           | 72.40           | 0.71|

Table 2: Results over the Wikipedia datasets.

| Models             | Artist PMR  | Artist Acc  | Artist LCS | NeurIPS PMR  | NeurIPS Acc  | NeurIPS LCS | τ |
|-------------------|-------------|-------------|------------|--------------|--------------|-------------|---|
| ALBERT-allpairs   | 1.14        | 29.37       | 66.15      | 0.34         | 26.69        | 64.12       | 0.54|
| ALBERT-adjonly    | 8.83        | 48.74       | 78.93      | 4.78         | 41.43        | 74.31       | 0.72|

Table 3: Cross-domain results, with finetuning over the Athlete dataset.

From Table 3, we can see that both ALBERT-adjonly and ALBERT-allpairs only experience marginal performance drops over Artist (similar topic), Athlete → Institution (topic change), Athlete → NeurIPS (topic and domain change).

3.6 Evaluation over Multi-document Summarisation

For multi-document summarisation, extractive document summarisation models extract sentences from different documents, not necessarily in an order which maximises discourse coherence. Thus, reordering the extracted sentences is potentially required to maximise the coherence of the extracted text.

We apply our proposed method to multi-document summarisation, in applying ALBERT-allpairs and ALBERT-adjonly to reorder sum-
We propose a simple yet effective training method to predict the relative ordering of sentences in a document, based on sentence adjacency and topological sort. Experiments on six datasets from different domains demonstrate the superiority of our proposed method, in addition to results in a cross-domain setting and for multi-document summarisation.

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|          | λ=0.0 | λ=0.3 | λ=0.5 | λ=0.7 | λ=1.0 |
|----------|-------|-------|-------|-------|-------|
| TextRank | 91.28 | 69.97 | 55.76 | 41.55 | 20.24 |
| allpairs | 91.02 | 70.88 | 57.45 | 44.03 | 23.89 |
| adjonly  | 91.94 | 71.76 | 58.30 | 44.85 | 24.67 |

Table 4: Coherence scores for reordered summaries. “allpairs” indicates ALBERT-allpairs and “adjonly” indicates ALBERT-adjonly (our model).
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