Abstract. Wavelet or quadrature mirror filter (QMF) satellites’ images are not commonly used in classification because of the modification in spectral responses that may confuse any classifier. Boundary pixels are hardly classified correctly in pixel-based classification especially in medium and coarse resolution. In such case, the sudden change in landcover is not measurable by the classifiers because the pixel may contain more than one class. This research work is a trial to investigate the proper enhancement in accuracy that may occur by using wavelet/QMF bands’ pyramids in classification instead of the original image bands. The reference map is prepared traditionally to measure the performance of the new system. The Wavelet/QMF image is constructed for each band of the satellite image. Then the classification is carried out for both the Wavelet/QMF image pyramid and the original satellite image using competitive learning neural networks (CLNN) method. The evaluation is carried out by comparing the classified Wavelet/QMF image with the classified original image. A statistical test is carried out to study the significance of using the classified Wavelet/QMF image in classification.

Keywords: remote sensing, classification, Wavelet/QMF pyramid, accuracy assessment.
is shown in Figure 2. The number of reforming pixels can be computed according to (Gonzalez et al., 2009) as:

\[ N^2 \left( 1 + \frac{1}{4^1} + \frac{1}{4^2} + \ldots + \frac{1}{4^P} \right) \leq \left( \frac{4}{3} \right) N^2, \]  

(1)

where \( N \) is the original image dimension in pixels and \( P \) is an integer number that determine the pyramid rank \((J-P)\) the pyramid rank. Figure 3 indicates the common image pyramids: Gaussian, Laplacian, wavelet and steerable pyramid.

On can deduct that Gaussian pyramid is blurred and subsampled form of the original image and it adds scale invariance to fixed-size image. The most common blurring filter used mostly is the mean filter. Laplacian pyramid shows the information added in Gaussian pyramid at each spatial scale and it can be used for noise minimization. Wavelet/QMF pyramid is sub band passed form with aliasing with non-oriented sub bands. It can be used for image enhancement. Steerable pyramid shows components at each size and orientation separately with no aliased sub bands. It is good for texture and feature analysis. But it is overcomplete and it has a high frequency residual form. In this research Wavelet/QMF pyramid with average filter is used due to it is the most used in most of remote sensing applications (Serwa, 2020b).

### 2. Methodology

The research is an investigation for the classification accuracy when using the full featured Wavelet/QMF pyramids in multispectral image classification. Landsat 8 MS image is used as an application. The reference of the study area is built in traditional way pixel by pixel to guarantee the reliable performance. All the main tasks such as: spatial sub setting, preparing regions of interest (ROIs), geo-referencing and corrections were done using ENVI software.
Construction of full featured Wavelet/QMF pyramid for each band of the satellite image bands is carried out using ADIPRS (Advanced Digital Image Processor for Remote Sensing) by Serwa (2009). The general classification approach described in Serwa and El-Semary (2020) is applied because it is well stabilized and dependable. This research is different from Serwa (2020b) which is a processing in the image domain while this is a processing in the frequency domain.

2.1. System overview

System overview can be abstracted using a flowchart diagram in Figure 4. The system begins with input of both the original satellite image bands and the reference. ENVI software is used to construct the main tasks such as: spatial sub setting, preparing regions of interest and georeferencing. While ADIPRS software is used to establish the full featured Wavelet/QMF pyramid and to adopt the classification for both the original image and the Wavelet/QMF image. The reference is used to measure the accuracy of the classification of both images (original and Wavelet/QMF). Unsupervised algorithm of competitive learning neural networks (CLNN) is used in this research because the reference was prepared using it previously.

Both classified original and classified Wavelet/QMF images are compared with the reference to examine the accuracy. A comparison between the accuracy of the classification of the original image and the accuracy of the classification of the Wavelet/QMF image is done. A statistical test is carried out to investigate the significance of using Wavelet/QMF pyramid in remote sensing classification.

2.2. Research data

Landsat 8 satellite image is used in this study which covers a part of Port Said city in Egypt with an area of 600×600 pixels (324 km²). The reference map is constructed normally by AutoCAD maps and suite visits (with GPSMAP device). The study area on ENVI environment is shown in Figure 5 before the subsetting.

Figure 6 shows the reference to obtain the best testing performance. One must note that each band of the
Figure 6. Reference for the study area

Figure 7. Construction of full featured Wavelet/QMF pyramid band
satellite image is used separately to produce its Wavelet/QMF pyramid and so the MS Wavelet/QMF pyramid is a composition of seven pyramid bands of the original image. The satellite image is corrected from all necessary errors such as atmospheric, radiometric and geometric corrections. Precautions were taken such as selecting the area with off-cloud and off-relief (no remarkable levels variation).

2.3. Processing

Figure 7 indicates the steps of construction of full featured Wavelet/QMF pyramid of single band of the MS image. Construction of full featured Wavelet/QMF pyramid band can be obtained in steps. The first step is establishing the fast wavelet transformed (FWT) image. A noise removal must be done to produces the denoised form. Then the reconstructed version can be obtained from the denoised form.

The absolute band can be obtained by subtracting the gray color from the denoised image. The last step is adding the absolute image to the original image band to finally obtain the full featured Wavelet/QMF image band. The previous steps are carried out for all 8 bands of the MS image. ADIPRS software is used to construct the full featured Wavelet/QMF pyramid. CLNN classification in its unsupervised form (clustering) is used with overfitting then make classless merging to obtain the required classes.

CLNN architecture is consisting of only input layer and output layer (without hidden layers) as shown in Figure 8. For more information about CLNN and its details see Serwa et al. (2010).

3. Results and analysis

The classification overall accuracy of 92% is obtained for the original image as shown in Figure 9. One must note the value of K-hat statistic (Kappa value) equals 90% and it is near the overall accuracy which means that the result is reliable. While Figure 10 shows the classification report of the Wavelet/QMF pyramid with overall accuracy of 93% and the value K-hat statistic is 92%. The last
results indicate an enhancement in classification due to the narrower gap between the overall accuracy and the value of K-hat statistic. One must search for a reason for the enhancement in classification accuracy when using the Wavelet/QMF pyramid. The reason can be explained as most of the miss-classified pixels are boundary pixels. So, the full featured Wavelet/QMF pyramid decreases the miss classification in the boundary pixels.

A comparison between the classification accuracy of the original classified image and the Wavelet/QMF classified pyramid must be carried out. The enhancement in accuracy is 1% which means initially that using the full featured wavelet/QMF pyramid is better. A statistical test is adopted to make sure this idea. Traditionally, 95% level of confidence can be assumed; so, the first hypothesis is that there is no significant difference between the two classification results while the alternative one is that there is a significant difference between them. The testing sample is 600x600 pixels > 30 pixels so that degree of freedom for is $\infty$ for both hypotheses. By comparing the two overall accuracies' percentages one can use F-test to evaluate the difference between them. The critical values can be retrieved from standard statistical tables showing the following:

$$F_{\text{Calculated}} = \frac{(0.93/0.92)}{(0.93/0.92)} = 1.011;$$

$$F_{\text{Critical}} = 1.0 \text{ (for degree of freedom } \infty \text{ for S1 and S2).}$$

So:

$$F_{\text{Calculated}} > F_{\text{Critical}} \text{ tables so the difference is significant.}$$

We must accept the hypothesis of there is a significant difference between the two results and reject the first one.

**Conclusions**

According to the research objective, using Wavelet/QMF image pyramid somewhat enhance the classification accuracy. The reason of the enhancement in classification accuracy can be explained by increasing the performance of the classifier concerning with the boundary pixel by making a true decision for. The full featured Wavelet/QMF pyramid solved the problem of the boundary pixels by make a sharp change in the spectral properties. The classifier reduces the confusion when examining the boundary pixels in the Wavelet/QMF pyramid. The research objective is achieved by indicating some unknown points
concerning with using the Wavelet/QMF pyramid in remote sensing classification.

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