An Efficient Cryptosystem Using Playfair Cipher Together With Graph Labeling Techniques

B Deepa¹, V Maheswari¹ and V Balaji²
¹Department of Mathematics, Vels Institute of Science, Technology and Advanced Studies, Chennai - 600 117, Tamilnadu, India.
²Department of Mathematics, Sacred Heart College, Tirupattur 635 601, Tamilnadu, India.

Corresponding Author: maheswari.sbs@velsuniv.ac.in

Abstract. Cryptography is the branch of Discrete Mathematics which deals with the transmission of secret communications between intended parties without the knowledge of third party. Graph theory is the enchanting field if Mathematics that designate integers to edges and vertices through some established functions. In current scenario security of communication plays a crucial role in any telecommunication or network applications. In this paper we have proposed an efficient cryptosystem using play fair cipher together with graph labeling to safeguard our secret text from unauthorised persons. Here we employ the substitution cipher namely Play fair cipher for plaintext encryption and our encrypted text in the form of Cipher Graph is forwarded to the receiver which on application of graph labeling yields our plaintext. Thus a fusion of the techniques Cryptography with Graph labeling provides ultimate security for secure transmission of data or information at various levels.

Keywords: Cipher Graph, Cipher key, Cipher text, Graceful edge labeling, Permutation Cipher, Plaintext, Play fair Cipher

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1. Introduction

In paper, [1], [2], [3], [4] Graph labeling techniques have been studied. We refer [5], [6],[7],[8] and [9] for Better Security Enhancement using Play fair Cipher. From [10] and [11] Permutation cipher techniques have been studied. [12], [13] and [14] showcases Encryption and Decryption techniques using various graphs. Inspired by [3],[4],[5],[7],[10],[11] & [12] we present an improved technique of coding a message based on Play fair Cipher and permutation for the graph using prime graceful labeling techniques. So here we make use of combination of Play fair and Permutation method to perform our encryption process after which we apply Graph labeling technique to pass the encrypted message to the receiver in a form Graph. Here we adopt symmetric key cryptosystem for the both process of encryption and decryption.

2. Definitions
**Definition 2.1: Graceful labeling**

G be a graph and \( f : V \rightarrow \{1, 2, 3, \ldots, p\} \) is an injective function. For each distinct edge \( e=uv \),

The induced edge labeling defined by \( f(uv) = |f(u) - f(v)| \) for all \( uv \in E \) is said to be Graceful labeling.

**Definition 2.2: Graceful graph**

A Graph which admits graceful labeling is said to be a graceful graph.

**Definition 2.3: plaintext**

A message is in the form of readable is known as plaintext

**Definition 2.4: Cipher Graph**

An encrypted message presented in the form of Graph is known as Cipher Graph.

**Definition 2.5: Permutation Cipher**

In Mathematics, The rearrangement of columns within a block is known as Permutation Cipher.

3. **Traditional Play Fair Cipher**

   Play fair cipher is the most popular symmetric polyalphabetic encryption technique. Instead of replacing single character in any kind of encryption process we can replace pair of character in play fair cipher encryption technique. It was invented in the year of 1854 by Charles Wheatstone but promoted and executed by Lord Play fair.

   The Traditional Play fair cipher uses a 5*5 matrix containing a keyword as shown in the table 1. Which consists of 25 cells. Firstly, the spaces of cell filled with letters of keyword then the rest of cells filled with English alphabets in the order, I and J sharing its position. The keyword together with the conventions for filling in the 5*5 matrix establish the cipher key. Here the keyword is “GREAT”

   ![Table 1](image)

4. **Proposed Algorithm For Encryption And Decryption Process**

   **Step: 1** Use a keyword “Mount” to generate Play Fair Cipher Matrix.

   **Step: 2** First take the message and Split it be a two letter block

   **Step: 3** Use the following Play Fair Cipher 8*8 matrix to encrypt message.
The Play fair encryption process has the following 4 rules.

Rule 1: If two letters are similar means we need to add on the letter “X” after the first letter.
Rule 2: In a Key table: 2 if two letters fall in the same row, Replace the two letters with their immediate right of their first letter.
Rule 3: In a Key table: 2 if two letters fall in the same column, Replace the two letters with their immediate bottom of their first letter.
Rule 4: In a key table: 2 if two letters neither fall on the same row or column, we need to connect the two letters by draw a rectangular or square format in a key table and replace by its corner letters.

Step: 4 Apply Permutation cipher (reordering the each character of cipher text I) for the encrypted message (Cipher text I) to constitute cipher text II.
Step: 5 Use Play fair Cipher 8*8 matrix to relate numerical value for the cipher text II to get cipher text 3.
Step: 6 For each character of Cipher text II, apply Additive 6 Caesar cipher to produce Cipher text III.
Step: 7 Use Graceful labeling technique to represent cipher text III in the form of Cipher Graph.

Decryption process follows all the steps of reverse encryption process 4.1:

Step: 1 Use Graceful labeling technique to trace Plaintext III.
Step: 2 Use Play fair Cipher 8*8 matrix to relate to trace numerical value of Plaintext II.
Step: 3 Use Permutation cipher to trace Plaintext I.
Step: 4 Use Play fair Cipher 8*8 matrix to finally trace our message.

5. Outline of Encryption and Decryption Process
6. Illustration 1

**Encryption Process 6.1:**

Let our Plaintext be “I like 5* Cadbury”.

**Stage 1 Proposed Play Fair Cipher 6.2:**

In our proposed methodology, the revised Play fair cipher utilized here is an 8*8 matrix which consists of keyword, upper and lower case of English alphabets, special characters and numerical values. We first insert the letter of the key word in the order followed by the remaining alphabets, numerical values, special characters in the order. Here the keyword is “Mount”.

| Table: 2 Play Fair Cipher 8*8 Matrix |
|--------------------------------------|
| M | o | u | n | t | A | B | C |
| D | E | F | G | H | I | J | K |
| L | N | O | P | Q | R | S | T |
| U | V | W | X | Y | Z | a | b |
|   | c | d | e | f | g | h | i | j |
|   | k | l | m | p | q | r | s | v |
| w | x | y | z | 0 | 1 | 2 | 3 |
| 4 | 5 | 6 | 7 | 8 | 9 | a | ! |
To encrypt our plaintext, we first split the plaintext be a two letter block.

**Table: 3 Two letter Block**

| I | l | i | k | e | 5 | * | C | a | d | b | u | r | y |

Now, the two letter block processed in play fair cipher matrix table 2,

Thus the plaintext “I like 5* Cadbury” encrypted as shown in the below table: 4.

**Table: 4 Cipher text 1**

| E | r | C | s | d | 6 | ! | B | v | i | W | C | m | l |

The plaintext processed in the play fair cipher will become our cipher text 1. Which is consider as a plaintext 1 to our next encryption process. Now we are going to use Permutation Cipher.

**Stage 2 Permutation Cipher 6.3:**

Permutation is a branch of Discrete Mathematics, is a rearrangement of the member into a sequence or ordered set. We can also referred as “linear order” or “arrangement of member”.

To encrypt our Plaintext 1, take the Plaintext 1 as a 2 letter 7 blocks, 

\[
\begin{pmatrix}
E c d ! v W m \\
6 B i C 1
\end{pmatrix}
\]

Then greater arrangements of the letter blocks according to the following permutation cipher \(1234567\).

The first 2 letter block moves to position 3, the second 2 letter block moves to position 1, the third 2 letter block moves to position 5, the fourth 2 letter block remains same in the position 4, the fifth 2 letter block moves to position 7, the sixth 2 letter block moves to position 2, the seventh 2 letter block moves to position 6. We get \(\begin{pmatrix}
c W E ! d m v \\
S C r B 6 1 i
\end{pmatrix}\).

After the permutation is applied the plaintext 1 will becomes cipher text 2 as shown in the below table: 5.
Further great use Play fair Cipher 8*8 matrix table 2, our cipher text 2 of “csWCer!Bd6m1vi” changed as numerical value as stated in table 6.

| c  | s  | W  | C  | E  | r  | !  | B  | d  | m  | l  | v  | i  |
|----|----|----|----|----|----|----|----|----|----|----|----|----|

The pair of number that coordinates of each letter in the table: 2,(I.e.) 51 stands for row 5 and column 1 so letter c, 67 stands for row 6 and column 7 so letter s, and so on.

| 51 | 67 | 43 | 18 | 22 | 66 | 57 | 17 | 52 | 83 | 63 | 76 | 68 | 57 |

The pair of number that coordinates of each letter in the table: 2,(I.e.) 51 stands for row 5 and column 1 so letter c, 67 stands for row 6 and column 7 so letter s, and so on.

| Row | 5 | 6 | 4 | 1 | 2 | 6 | 5 | 1 | 5 | 8 | 6 | 7 | 6 | 5 |
|-----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| column | 1 | 7 | 3 | 5 | 8 | 2 | 6 | 7 | 7 | 2 | 3 | 3 | 6 | 8 | 7 |

Here we divide the pair value by row and column to represent the numeric value in the cipher graph. Finally our row and column value of cipher text 3 presented in the form of Cipher Graph. Then the Cipher Graph is shared to the receiver along with the following clues.
Clue 6.4:

**Key: 1** Use Graceful labeling formula to trace edges which the receiver make arrangements in the order of

| Row  | ! | ~ | * | ) | ( | ~ | ! | ! | & | ~ | # | ~ | ! |
|------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Column | ) | # | ^ | & | ( | ~ | # | # | ( | ^ | ~ | & | # |

**Key: 2** Use Key table 8*8 matrix to know alphabetic value.

**Key: 3** Use permutation cipher to make the arrangement of the block in the order

\[
\begin{pmatrix}
1 & 2 & 3 & 4 & 5 & 6 & 7 \\
3 & 1 & 5 & 4 & 7 & 2 & 6 \\
\end{pmatrix}
\]

**Key: 4** Use Play fair cipher to finally trace our message.

**Decryption Process 6.5:**

The Decryption is the progress of transforming cipher text back to plaintext. For the above cipher Graph the receiver has to find the edges by applying the formula of Graceful Labeling thus obtained forms our Plaintext in the form of Graph.

**Fig: 3 Shadow Graph**

![Graph Image](image-url)
We obtain plaintext 3, further arrangements of edges in the order as stated in clue 1 as shown below table 8.

| Row | 5 | 6 | 4 | 1 | 2 | 6 | 5 | 1 | 5 | 8 | 6 | 7 | 6 | 5 |
|-----|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| column | 1 | 7 | 3 | 8 | 2 | 6 | 7 | 7 | 2 | 3 | 3 | 6 | 8 | 7 |

The row and column value combined as a pair of number, by locating each pair value in the table 2, i.e. 51 stands for row 5 and column 1 so letter c, 67 stands for row 6 and column 7 so letter s, and repeating this similar process which yield our Plaintext 2 as shown in the below table 9.

| Table: 9 Plaintext 2 |
|---------------------|
| c | s | W | C | E | r | ! | B | d | 6 | m | 1 | v | i |

Rewriting the each block corresponding to permutation cipher stated in clue 3, we get Plaintext 1 as shown in the below table 10.

| Table: 10 Plaintext 1 |
|-----------------------|
| E | r | C | s | d | 6 | ! | B | v | i | W | C | m | 1 |

Further considering Play fair Cipher we get our Plaintext.

Finally, we reach our message is “I like 5* Cadbury”.

7. Illustration 2

Encryption Process 7.1:

Let us consider our Plaintext be “Catch up!”.

For the encryption process, we first divide the plaintext into two letter block as shown in table 11.
Now, the two letter block processed in play fair cipher matrix 9*9 as stated in the below table

| Table: 11 Two letter block |
|----------------------------|
| C | a | t | c | h | u | P | ! |

Now, the two letter block processed in play fair cipher matrix 9*9 as stated in the below table 12,

| Table: 12 Play fair Cipher 9*9 matrix |
|---------------------------------------|
| W | o | n | d | e | r | A | B | C |
| D | E | F | G | H | I | J | K | L |
| M | N | O | P | Q | R | S | T | U |
| V | X | Y | Z | a | b | c | f | g |
| h | i | j | k | l | m | p | q | s |
| t | u | v | w | x | y | z | 0 | 1 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | ! |
| ~ | @ | # | $ | % | ^ | & | * | ( |
| ) | { | } | [ | ] | \ | | : | “ |

Thus the plaintext “Catch up!” encrypted as “egzvits8”. Now, we get our cipher text 1 in the form of two letter block as stated in below table 13.

| Table: 13 Cipher text 1 |
|-------------------------|
| e | g | z | v | i | t | s | 8 |

The plaintext processed in the play fair cipher 9*9 matrix will become our cipher text 1. Which is taken as a plaintext 1 to our next encryption process of permutation cipher.

First, to encrypt our Plaintext 1, take the Plaintext 1 as a 2 letter 4 blocks,

\[
\begin{pmatrix}
  e \\
  z \\
  i \\
  s
\end{pmatrix}
\begin{pmatrix}
  g \\
  v \\
  t \\
  8
\end{pmatrix}
\]
Then greater arrangements of the letter blocks according to the following permutation cipher

\[
\begin{pmatrix}
1 & 3 & 4 & 2 \\
4 & 2 & 3 & 1
\end{pmatrix}
\]

We get,

\[
\begin{pmatrix}
z & i & s & e \\
v & t & 8 & g
\end{pmatrix}
\]

The first block moves to position 4, the second block moves to position 1, the third block moves to position 2, the fourth block moves to position 3. Further, the greater arrangements of plaintext 1 using permutation cipher will become cipher text 2 as shown in the below table 14.

**Table: 14 Cipher text 2**

| z | v | i | t | s | 8 | e | g |
|---|---|---|---|---|---|---|---|

Then cipher text 2 of “zvits8eg” value taken from the Play fair cipher 9*9 matrix table 12, as shown in table 15.

**Table: 15 Cipher text 3**

| 67 | 63 | 52 | 61 | 59 | 77 | 15 | 49 |
|---|---|---|---|---|---|---|---|

The pair value which indicates each letter in the table 12, i.e. 67 stands for row 6 and column 7 so letter z, 63 stands for row 6 and column 3 so letter v, and so on.

**Table: 16 Row and Column value of Cipher text 3**

| Row | 6 | 6 | 5 | 6 | 5 | 7 | 1 | 4 |
|-----|---|---|---|---|---|---|---|---|
| Column | 7 | 3 | 2 | 1 | 9 | 7 | 5 | 9 |
Now, we split up the pair value by row and column to present in the cipher graph. Finally our row and column value of cipher text 3 presented in the form of Cipher Graph. Then the Cipher Graph send to the receiver with the following clues.

**Fig: 4 Cipher Graph**

```
| Row | # | # | * | # | * | @ | ! | ^ |
|-----|---|---|---|---|---|---|---|---|
| Column | @ | & | ( | ! | $ | @ | * | $ |
```

**Clue7.2:**

**Key: 1** Use Graceful labeling formula to trace edges which the receiver make arrangements in the order of

**Key: 2** Use Key table Play fair cipher 9*9 matrix to know alphabetic value.

**Key: 3** Use permutation cipher to make the arrangement of the blocks in the order

\[
\begin{pmatrix}
1 & 3 & 4 & 2 \\
4 & 2 & 3 & 1
\end{pmatrix}
\]

**Key: 4** Use Play fair cipher to finally trace our message.
Decryption Process 7.3:

In Decryption process, first the receiver has to find the edges for the above Cipher Graph by applying the formula of Graceful Labeling thus obtained forms our Plaintext in the form of Graph as shown in below.

![Fig 5: Tower Graph](image)

Further arrangements of edges in the order as stated in clue 1, we obtain Plaintext 3 as shown in the below table 17.

| Table: 17 Row and Column value of Plaintext 3 |
|---------------------------------------------|
| Row | 6  | 6  | 5  | 6  | 5  | 7  | 1  | 4  |
| Column | 7  | 3  | 2  | 1  | 9  | 7  | 5  | 9  |

The row and column value combined as a pair of number, by locating each pair value in the table 12, i.e. 67 stands for row 6 and column 7 so letter z, 63 stands for row 6 and column 3 so letter v, and repeating this similar process Which yield our Plaintext 2 as shown in the below table 18.
Further greater arrangements of two letter block corresponding to permutation cipher stated in clue 3 will give us plaintext 1 as stated in the below table 19.

**Table: 18 Plaintext 2**

| z | v | i | t | s | 8 | e | g |
|---|---|---|---|---|---|---|---|

Further plaintext 1 processed in Play fair Cipher matrix 9*9 which yield our initial Plaintext.

Finally, we obtain our message is “Catch up!”.

8. Conclusion

Cryptography is a method of securing information and communication from malicious third parties. The modification of play fair cipher with different size matrix along with Graceful labeling techniques will give us more integrity and security to the communication. In future work we can try with further extension and modification of matrix size along with some different labeling techniques.

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