Thin layers of topological insulator materials are quasi-2D systems featuring a complex interplay between quantum confinement and topological band structure. To understand the role of the spatial distribution of carriers in electrical transport, the Josephson effect, magnetotransport, and weak antilocalization are studied in bottom-gated thin Bi₂Te₃ topological insulator films. The experimental carrier densities are compared to a model based on the solutions of the self-consistent Schrödinger–Poisson equations and they are in excellent agreement. The modeling allows for a quantitative interpretation of the weak antilocalization correction to the conduction and of the critical current of Josephson junctions with weak links made from such films without any ad hoc assumptions.

3D topological insulators (3D TIs) are a relatively new class of semiconductor materials with a band inversion in the bulk band structure. The energetic ordering of orbitals that create valence and conduction bands is reversed and surface states emerge that are protected by the topology of the band structure. These surface states feature a Dirac-like energy dispersion with a spin structure that is linked to the crystal direction (“spin-momentum-locking”). Topological quantum states are predicted to generate new low-energy effective modes of the electronic system, Majorana bound states, when topological surface states (TSS) are coupled to conventional s-wave superconductors. The Majorana bound states in condensed matter systems could potentially be used as topological qubit to perform fault-tolerant computation. Recently, signatures of Majorana fermions have been found in quantum structures based on 2D and 3D topological insulator (TI) Josephson devices.

While Bi₂Te₃ and other Bi-based TIs have the advantage of significantly larger bandgaps (several 100 meV), and although proximity-induced superconductivity in Josephson devices fabricated on thin films of these materials have been reported, little is known about the spatial distribution of carriers in normal state transport and induced supercurrent. A nonuniform charge distribution of intrinsic dopants and extrinsic impurity contaminations are known to be present in Bi-based TI films, causing band bending close to interfaces. These effects also need to be taken into consideration in the discussions of proximity effects in these materials. Using thinner samples would minimize the contribution of bulk modes in electronic transport by decreasing the total number of dopant charges. However, when the sample thickness approaches the length scale of electrostatic screening or becomes comparable to the typical spreading of the TSS wave function into the bulk, the coupling between the superconductor and the TI material could change substantially.

To address the above effects, we study electrical transport in thin Bi₂Te₃ films with small, but finite, residual doping. Unlike the compound Bi₂Se₃, the Bi₂Te₃ material is not prone to having a large number of surface vacancies that lead to the formation of deep quantum wells at the surfaces. This allows us to observe the nontrivial interplay between band bending in the bulk and the surface states, resulting in a partial decoupling of the latter. We compare devices prepared from thin films of average thicknesses 6 and 15 nm. The choice of 6 nm for the thinner film is motivated by the objective of eliminating most of the TI bulk without opening a hybridization gap. As we use a bottom gate to modulate electrical transport properties, the value for the thicker film is chosen to be comparable to the electrostatic screening length of the films (bulk screening length estimated to be in the range of 10 to 30 nm).

First, we observe an unusual gate-voltage dependence of the critical current in Josephson junctions and find that it does...
not scale with the carrier densities obtained from Hall effect measurements. Second, to understand the unusual gate-voltage dependence of transport properties, we calculate self-consistently the gate-dependent carrier distributions for a tight-binding model of the film and vary the doping levels and surface charges. A uniform dopant distribution yields the best fit with the Hall effect data. Lastly, backed by the theoretical model, we are able to interpret the magnitude of the observed weak antilocalization correction to the conductivity quantitatively and conclude that the critical current of the Josephson devices maps the change in shape of the (sub)band structure of the thin film when a gate voltage is applied.

High-quality thin films of Bi$_2$Te$_3$ were grown by molecular beam epitaxy (MBE). Hall bar devices and Josephson junctions were patterned side-by-side using standard electron-beam lithography, and subsequent dry etching and sputter deposition of electrodes. Further details on the growth procedure of the thin films and device fabrications are presented in Supporting Information and refs. [24, 25].

Figure 1a shows a typical Nb/Bi$_2$Te$_3$/Nb Josephson junction (JJ6/1). The weak link is 860 nm wide and 250 nm long. The device was patterned on a 6 nm-thick Bi$_2$Te$_3$ film, which was grown on a (111)-oriented SrTiO$_3$ (STO) substrate. The current–voltage characteristic (IVC) is plotted in Figure 1b. The device exhibits sharp switching into the voltage state with little hysteresis. It displays a Fraunhofer-like Josephson diffraction pattern with perpendicular applied magnetic field (Figure 1c), which indicates a uniform critical current density in the weak link. When irradiated with microwaves of frequency $f = 6.02\,\text{GHz}$, the IVC develops voltage plateaus corresponding to multiples $n$ of the driving frequency

$$V_n \approx n \times (12.4\,\mu\text{V})$$

where $h$ and $e$ are Planck’s constant and the elementary charge, respectively (Figure 1d). Both, even-$n$ and odd-$n$ steps, are present in these Josephson devices.

We have modulated the charge carrier distributions in the films by electrostatic gating. We have used the STO substrate as the back-gate dielectric since it has a high dielectric constant ($\varepsilon_{\text{STO}} \approx 2-6 \times 10^4$) at low temperature.[27] Voltages $V_{\text{bg}}$ in the range of ±200 V are sufficient to create a triangular quantum well or to deplete carriers in the bottom region of the film.[28] Figures 2a and 2b depict the effect of charge (re-)distribution in the material on the Josephson effect for two representative Josephson junctions that were patterned on films of 6 nm (JJ6/1) and 15 nm (JJ15/1), respectively. At 200 V gate bias, the Josephson coupling energy amounts to $\varepsilon_{\text{JJ}} = 18\,\mu\text{eV}$ for both devices. The Josephson critical current $I_c$ is defined by the voltage criterion $V \leq 1\,\mu\text{V}$. An estimate of the normal state resistance of the device is obtained from a fit to the IVC at large current bias ($>1.5\,\mu\text{A}$). The gating characteristics of the devices are identical. At large negative gate bias,
$I_c$ is approximately constant. For positive gate voltage, it rises sharply at first, then grows with a smaller slope at high bias. In this region, the current–voltage characteristic of device JJ15/1 shows larger hysteresis and stochastic switching (Figure 2b). For the values of $I_c$ and $R_N$, the hysteresis is expected to arise from the phase dynamics, not the (geometric) capacitance of the weak link. The normal state resistance $R_N$ drops monotonously with increasing gate voltage. In the transition region around $V_{bg} = 0$, the decrease is more prominent.

Next, we compare the gating behavior of $I_c$ with the evolution of the charge carrier densities in the film. We have performed magnetoresistance measurements as a function of back-gate voltage on a Hall bar device fabricated on the same 15 nm-thick film as the JJ15/1 device for a sample temperature of 50 mK. The Hall data were fitted with a standard two-carrier model expression for $R_{xy}$ using the zero-field sheet resistance $R_S$ as a constraint (Figure S1a, Supporting Information).

Figure 3a (black filled squares) gives the total carrier density $n$ as function of gate voltage. Similar to the critical current data, saturation at $2.2 \times 10^{13}$ cm$^{-2}$ in the depletion region was observed and a carrier density increase for positive gate bias with a slope change around 60 V and a maximum value of $5.3 \times 10^{13}$ cm$^{-2}$ at 200 V. The mobilities of the two carrier types change only slightly with gate voltage. The extracted high- and low-mobility carriers are $\approx 1900$ cm$^2$ V$^{-1}$ s$^{-1}$ and $\approx 700$ cm$^2$ V$^{-1}$ s$^{-1}$, respectively.

To understand the charge distribution in the films at different gate voltages, we have modeled the band structure of a 15 nm-thick film of Bi$_2$Te$_3$ using a tight-binding Hamiltonian with parameters from ref. [30]. To determine the correct doping level, a series of solutions to the coupled Schrödinger and Poisson equations were calculated self-consistently using the NEMO5 software package. For each series, the chemical potential and the top surface electrostatic potential were kept fixed and the bottom electrostatic potential was varied. Then, we have calculated the carrier density at the Fermi level and the (approximate) back-gate voltage. Representative cuts of the band structure between points of high symmetry along

![Figure 2](image1.png)

**Figure 2.** a,b) Back-gate voltage dependence of the normal state resistance and the Josephson critical current measured at 15 mK for Nb/Bi$_2$Te$_3$/Nb junctions of 6 nm (JJ6/1) (a) and 15 nm (JJ15/1) (b) thickness of the Bi$_2$Te$_3$ weak link. We find that the critical current is enhanced for positive back-gate voltages, it flattens out when negative gate bias is applied. For both devices, the normal state resistance $R_N$ drops by a factor of $n \geq 2.2$ with increasing gate voltage.

![Figure 3](image2.png)

**Figure 3.** Carrier density, weak antilocalization fit data, and modeling of the carrier distribution in a 15 nm thick Bi$_2$Te$_3$ film. a) The total carrier density as a function of gate voltage from Hall measurements (black filled squares), and from band structure modeling (red filled circles). The open red circles at high voltages are obtained by excluding disconnected hole pockets close to the M point of the band structure from the summation. b) Prefactor $\alpha$ and dephasing length $l_\phi$ from a fit to the weak antilocalization correction of the conductance. A clear increase in the magnitude of the weak localization signal indicates the decoupling of the bottom TSS from the bulk.
the line K−Γ−M are plotted in Figure S2a–c, Supporting Information. (For details on calculations, see Supporting Information.) Figure 3a shows good agreement between experimental data (black filled squares) and extracted carrier densities of the model calculation (red filled circles) for a chemical potential shift of 300 meV and a top surface electric voltage of −0.3 V. These parameters concur with results of ARPES measurements on Bi2Te3 films of the same growth series with identical growth parameters.\[35\] The discrepancy at higher gate voltages is resolved by excluding disconnected hole pockets near the M-point of the Brillouin zone from the carrier density estimate (open circles in Figure 3a). We have found that the presence of TSS makes it difficult to deplete transport carriers, it is easy to enlarge the Fermi surface by applying a small positive gate bias.

Electrostatic gating changes the shape of the confining potential and the distribution of transport carriers in the well. Consequently, as a function of gate bias, different sections of the film participate in transport. Depending on the effective scattering length of the defect potentials, the disorder potential landscape of each section may be different. The scattering rate between the sections depends on the wavefunction overlap. We have observed the effect experimentally as a gradual increase in the weak antilocalization (WAL) correction to the longitudinal resistance of the Hall bar structures. To quantify the change, we have fitted the magnetococonductance data (Figure S1b, Supporting Information) to the Hikami–Larkin–Nagaoka (HLN) formula:\[32,33\]

\[
G - G_b = \alpha \frac{e^2}{2\pi h} \left[ \ln \left( \frac{\hbar}{4e^2l_p^2} \right) - \Psi \left( \frac{1}{2} + \frac{e^2}{4\hbar l_p^2} \right) \right]
\]

(1)

after subtracting a quadratic background \(G_b\). Here, \(\Psi\) denotes the digamma function. Figure 3b depicts the back-gate voltage dependence of prefactor \(\alpha\) and the dephasing length \(l_p\), quantities that characterize the magnitude of the correction and the length scale of electronic phase coherence, respectively. The dephasing length was found to be \(\approx 0.8\ \mu m\) to either side of the transition but dips to \(\approx 0.48\ \mu m\) in between. At large positive gate bias, the prefactor \(\alpha\) is \(\approx 1.1\) and increases to \(\approx 1.7\) at large negative gate voltage. The transition occurs gradually in the same bias region where we have observed a decrease in the Josephson critical current.

The spatial redistribution of charge carriers allows for a partial decoupling of transport on the bottom surface. Naively, one might expect an increase in the WAL signal as scattering between the TSS and the bulk is suppressed, and a separate conduction channel forms. A semi-quantitative interpretation of the magnitudes of the correction, however, requires a detailed analysis of the number of Cooperon modes (interference contributions to weak (anti-)localization) in the thin film.\[14\] The two relevant limits are: Firstly, a system of coupled TSS and bulk quantum well states (QWS) in the limit of dephasing time much larger than spin and valley (“top” or “bottom”) scattering time\[35\] for which two (hybridized) spin-singlet bulk Cooperon modes exist (\(e^2/h\) correction), explaining the observed increase of the weak antilocalization signal for sample depletion. The smooth transition between the two regimes is governed by the characteristic resistances of the bulk QWS and TSS channels. They are set by the dephasing lengths in the respective channels which change with the hybridization of Cooperon modes. Decoupling of the TSS is then observed as a rebound in the dephasing length to its larger, initial value at the lowest gate voltages (Figure 3b).

The experimental data are in good qualitative agreement with the theoretical scenario.\[14\] Deviations may arise, for example, from additional corrections which are specific to topological surface states and modify the HLN expression.\[36\]

Finally, using the band structure model of the thin film, we could understand the strong enhancement of the Josephson critical current that surpasses the increase in charge carriers multiple times. As all Josephson devices have \(eI_{R_N}\)-products significantly smaller than the bulk pairing potential in the Nb electrodes (\(\Delta = 1.3\ \text{meV}\) estimated from the critical temperature of the Nb electrodes), and \(I_c\) varies slowly with temperature (Figure 4a), the devices are superconductor–normal

![Figure 4](image-url)

**Figure 4.** Critical current of Josephson devices with 15 nm-thick Bi2Te3 weak links. a) Temperature dependence of the critical current in JJ15/1 for different gate voltages. A fit to the high temperature data was performed to estimate the magnitude of the Thouless energy (dashed lines). b) Critical current of devices JJ15/1 and JJ15/2 at different gate voltages. The open symbols represent experimental values. The solid lines are obtained from band structure data using a single scaling factor for the entire gate voltage range. Stochastic switching sets in above \(\approx 120\ \text{nA}\).
metal–superconductor (SNS) contacts in the diffusive, long junction regime. The electronic phase coherence limits the critical current, and the scale of the Josephson energy is set by the Thouless energy \( (R_C) \) of electrons traversing the weak link: 
\[
e I, R_N \approx E_C \left[ L_c / L_t \right] \exp\left(-L_c / L_t \right)
\]
valid for \( T \gg 5E_C / k_B \). Here, \( L_t \) is the thermal coherence length \( L_t = \sqrt{\hbar D / 2\mu k_B T} \) and \( L_c \) the length of the junction. We have obtained values of \( E_C = 4.3 - 6.6 \) μeV. To understand the gating behavior of \( I_c \), we have calculated the average diffusion constant \( D \) from the model band structures (for details on calculations, see Supporting Information). Figure 4b (solid lines) shows calculated critical current for two junctions with 15 nm-thick Bi\textsubscript{2}Te\textsubscript{3} weak links. The shapes of the \( I_c = V_{th} \) curves are very well reproduced. The scaling factor is two orders of magnitude larger than the theoretical value in ref. [39], but it compares well with the reported suppression of critical current in graphene Josephson devices.[40] However, we provide a different interpretation. In ref. [40], the discrepancy is attributed to the interface resistance between the electrodes and the graphene. For devices presented in this work, the contact resistance is estimated to be about 20% of \( R_N \). The reduction in \( I_c \) should thus be attributed to additional scattering centers due to the damage incurred during device fabrication. Unlike graphene, the added defects facilitate scattering between \( \approx 20 \) bands, hence the significant increase in scattering frequency and a smaller critical current. In our experiments, there is no indication of the decoupled bottom surface contributing to the supercurrent transport. A possible explanation is that the carrier density on the bottom surface is very small compared to the bulk subbands. Further, the depletion zone acts as additional barrier for Cooper pair tunneling.

In summary, we have studied the gate-dependence of the Josephson effect, the carrier densities, and the weak anti-localization correction to the conductivity in devices fabricated from thin Bi\textsubscript{2}Te\textsubscript{3} films. While the carrier densities were enhanced by applying positive gate voltages, the samples could not be depleted. This was explained by calculating the carrier distribution in the thin film self-consistently using a tight-binding model. The theoretical calculation has reproduced the experimental values for the transport carrier densities well. While positive gate voltages created a potential well, negative gate bias formed a depletion zone in the material. This scenario was corroborated by the analysis of the WAL signal in magnetotransport measurements. The Josephson devices were found to be in limit of long, diffusive SNS junctions, and the critical current scaled with the estimated Thouless energy obtained from a calculation of the average diffusion constant in the band structure model.

We conclude that a satisfactory description of all transport experiment on the Bi\textsubscript{2}Te\textsubscript{3} thin film devices could be found by taking the carrier distribution in the sample and the shape of the sub-bands into account. The evolution of the carrier density with applied gate voltage followed naturally from the profile of the electrostatic potential in the film, and no ad hoc assumptions about the charge distribution in the sample or the capacitance of surface and bulk states were required. In particular, we want to stress that for a careful evaluation of the WAL signal, we cannot simply interpret it as a sum of topological surface states and bulk, but must look at the probabilities of scattering between different two-dimensional electron systems and the resulting corrections to the conductivity. Ultimately, from a careful, systematic analysis, we are able to reveal that the critical current in TI Josephson devices maps band structure properties of the thin films. These data thus provide a coherent picture that incorporates band bending in the discussion of proximity effects for 3D TI devices. We like to finish by stressing that this analysis could be extended to discuss proximity superconductivity in other TI and narrow gap semiconductor systems for which band bending plays a role.

Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest
The authors declare no conflict of interest.

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