Determination of the $\eta'$-proton scattering length in free space

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Taking advantage of both the high mass resolution of the COSY–11 detector and the high energy resolution of the low-emittance proton-beam of the Cooler Synchrotron COSY we determine the excitation function for the $pp \rightarrow ppp'\eta'$ reaction close-to-threshold. Combining these data with previous results we extract the scattering length for the $\eta'$-proton potential in free space to be $\text{Re}(a_{pp'}) = 0 \pm 0.43\text{ fm}$ and $\text{Im}(a_{pp'}) = 0.37^{+0.40}_{-0.16} \text{ fm}$.

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In this letter we report the determination of the scattering length for the interaction of the $\eta'$ meson with the proton based on the shape of the excitation function for the $pp \rightarrow ppp'\eta'$ reaction measured close to the kinematic threshold. Using the high mass resolution of the updated COSY–11 detector and the low-emittance proton-beam of the Cooler Synchrotron COSY the excitation function was determined down to excess energy $Q = 0.76$ MeV above threshold, with the precision $\Delta Q = 0.1$ MeV improved by more than a factor of five with respect to previous measurements. The improved resolution enabled quantitative extraction of the $\eta'$ proton scattering length in free space.

The scattering lengths describing interaction potentials between mesons and nucleons are of fundamental importance in hadron physics. However, they are not well established especially for those flavor neutral mesons that are characterized by very short life times making investigations of the meson-nucleon potential in the standard way via scattering experiments impossible. So far, based on the shift and width of the ground state of pionic hydrogen atoms, only the scattering length of the $\pi^0$-nucleon potential is accurately determined with a precision of about 0.001 fm. The scattering length for the $\eta$-nucleon potential is determined more than two orders of magnitude less precisely, with phenomenological values quoted for the real part between ~0.2 fm and ~1 fm depending on the analysis method. Until now the $\eta'$-nucleon scattering length had been estimated only qualitatively.

Measurements of the $\eta$- and $\eta'$-nucleon and nucleus systems are sensitive to dynamical chiral and axial U(1) symmetry breaking in low energy QCD. While pions and kaons are would-be Goldstone bosons associated with chiral symmetry, the isosinglet $\eta$ and $\eta'$ mesons are too massive by about 300-400 MeV for them to be pure Goldstone states. They receive extra mass from non-perturbative gluon dynamics associated with the QCD axial anomaly. This OZI violation is also expected to influence the $\eta'$-nucleon interaction. Without the gluonic mass contribution the $\eta'$ would be a strange quark state after $\eta$-$\eta'$ mixing (and the $\eta$ would be a light-quark state degenerate with the pion), mirroring the situation with isoscalar $\phi$ and $\omega$ vector mesons. To the extent that coupling to nucleons and nuclear matter is induced by light-quark components in the meson, any observed scattering length and mass shift in medium is induced by the QCD axial anomaly that generates part of the $\eta'$ mass.

In COSY–11 the $\eta'$ meson was produced in $p-p$ collisions of the COSY proton beam with an internal hydrogen cluster target. The four-momenta of outgoing protons from the $pp \rightarrow ppX$ reaction were measured in two drift chambers and scintillator detectors and the $\eta'$ meson was identified via the missing mass technique. The low emittance proton beam combined with the high missing mass resolution of the COSY–11 detector allowed measurements very close to the kinematic threshold where the signal-to-background ratio increases due to the more rapid reduction of the phase space for multimeson than for single meson production. The measurement was conducted at five excess energies in the range $Q = 0.76$ MeV to $Q = 4.78$ MeV. The determination of the absolute value of $Q$ was based on the position of the $\eta'$ signal in the missing mass spectra. (A typical missing mass spectrum is shown in the top plot of Figure). $Q$ was determined with a precision of 0.10 MeV, where 0.06 MeV is due to the uncertainty of the $\eta'$ meson mass and 0.04 MeV comes from the possible misalignment of the relative setting of the detection system components and the center of the region.
of the beam and target overlap. The latter was monitored by the measurement of elastically scattered protons \( \text{[1]} \). The experiment was designed to reduce the spread of excess energy to a negligible level by the use of a rectangular collimator in the target setup so the width of the target stream was equal to 0.90 mm while crossing the proton beam. Due to the known dispersion of the COSY beam, this width is equivalent to an effective beam momentum spread of \( \pm 0.06 \text{ MeV/c} \) corresponding to 0.02 MeV spread of excess energy \( Q \). The size of the target stream was monitored by a dedicated wire device with an accuracy of 0.05 mm \( \text{[12]} \) and in addition it was controlled independently by measuring elastically scattered protons. The number of registered \( pp \rightarrow pp \) events as a function of the protons scattering angle together with the known differential cross section for this process \( \text{[13]} \) allows total luminosity determination as presented in the bottom plot of Figure 1. The luminosity was determined for each beam momentum separately. The total luminosity for all measurements amounts to about 2.55 pb\(^{-1}\). Due to the high statistics of the detected \( pp \rightarrow pp \) events, the error in the determination of luminosity is less than 0.05% and can be neglected in the analysis below. Here we conservatively take the systematic uncertainty of the data from the EDDA Collaboration used for the normalization \( \text{[13]} \). The number of identified \( \eta' \) mesons was derived from fit of the simulated missing mass spectra to the experimental ones after background subtraction (see the top plot of Figure 1) with the normalization as the only free parameter. The background was determined experimentally \( \text{[3, 12]} \). The geometrical acceptance and reconstruction efficiency for the \( pp \rightarrow pp\eta' \) process were estimated based on simulations including experimentally determined properties of the COSY–11 detector \( \text{[1]} \) and taking into account the final state interaction (FSI) of the outgoing protons \( \text{[4]} \). Final results with statistical and systematic uncertainties are collected in Table I and shown in Figure 2. Systematic uncertainties were estimated taking into account differences in the final result obtained by (i) applying different methods of events counting, including variation of the range used for the background and signal counting and various binnings (3%), (ii) different methods of background subtraction (7%) \( \text{[8]} \), (iii) taking into account possible geometrical misalignment of the relative positions of the detection system components (2%), (iv) uncertainty in the reconstruction efficiency of two close proton tracks (9%) \( \text{[14]} \), and (v) the relative uncertainty in the EDDA data sets used for the luminosity determination (2.5%). Because of the very small excess energies, the variation of the result due to different models of the proton-proton FSI (see Figure 3) was found to be negligible.

Based on the data from previous experiments \( \text{[14, 20]} \) and the close to threshold total cross sections reported in Table I we have extracted the \( \eta' \)-proton scattering length. To this end the experimental excitation function

![Figure 1: Results obtained for beam momentum of 3210.7 MeV/c corresponding to \( Q = 0.76 \text{ MeV} \). Top: Missing mass spectrum from experimental data (dots), and simulations (histogram). The simulated spectrum was normalized to the data. Bottom: Open points indicate the number of measured events of elastically scattered protons. Solid points denote fit result of differential cross sections determined by the EDDA Collaboration \( \text{[13]} \) with luminosity as the only free parameter.](attachment:figure1.png)

| \( Q [\text{MeV}] \) | \( \sigma(pp \rightarrow pp\eta') [\text{nb}] \) |
|-----------------|------------------|
| 0.76 \( \pm 0.10 \) | 1.38 \( \pm 0.08 \) \( \pm 0.17 \) |
| 1.35 \( \pm 0.10 \) | 3.82 \( \pm 0.19 \) \( \pm 0.47 \) |
| 1.66 \( \pm 0.10 \) | 4.97 \( \pm 0.28 \) \( \pm 0.61 \) |
| 2.84 \( \pm 0.10 \) | 11.41 \( \pm 0.40 \) \( \pm 1.39 \) |
| 4.78 \( \pm 0.10 \) | 17.58 \( \pm 0.64 \) \( \pm 2.15 \) |

Table I: Cross sections for the \( pp \rightarrow pp\eta' \) reaction at the five measured excess energies. The excess energy \( Q \) is tabulated with the absolute systematic uncertainty and the cross section values are given with the statistical and systematic uncertainties, respectively.
The superimposed curves show results of fits with the η′-proton scattering length as a free parameter and parametrizing the pp-FSI enhancement factor as in Refs. \[23\] (thick dashed line), inverse of the squared Jost function \[22\] (thin solid line) and Niskanen-Goldberger-Watson model \[23\] (thin dashed line). The thick dashed line is shown only in the range of applicability of the formula used for the enhancement factor \[24\]. For comparison the thick solid line shows result of the fit obtained for the whole Q range with pp-FSI parametrization from Ref. \[22\]. The small plot shows the excitation function up to \(Q = 180\) MeV where the thin solid and thin dashed curves overlap.

for the \(pp \rightarrow pp\eta'\) reaction was compared to the results of calculations taking into account proton-proton and η′p interactions, where the real and imaginary parts of the η′p scattering length were varied as free parameters. At threshold the distance probed by the \(pp \rightarrow pp\eta'\) reaction is determined by the momentum transfer between colliding nucleons and equal to about 0.2 fm, whereas the typical range of the strong nucleon-nucleon or meson-nucleon interaction is of the order of a few Fermi. In addition the energy range considered in this article is two orders of magnitude smaller than the four-momentum transfer (1 GeV) governing the production amplitude. Therefore, the calculations were carried out using a Watson-Migdal approximation \[21\] and the complete transition matrix element of the \(pp \rightarrow pp\eta'\) reaction was factorized as

\[
|M_{pp\rightarrow pp\eta'}|^2 \approx |M_0|^2 \cdot |M_{FSI}|^2 .
\]

Here \(|M_0|^2\) represents the total short range production amplitude and \(|M_{FSI}|^2\) denotes the final state interaction enhancement factor. Exact Faddeev calculations for the dynamics of three-body \(pp\eta'\) final states are unavailable.

Therefore, the enhancement factor for the \(pp\eta'\) system was approximated assuming the factorization of \(M_{FSI}\) into two-particle scattering amplitudes \[22\].

\[
M_{FSI} = M_{pp}(k_1) \times M_{p1\eta'}(k_2) \times M_{p2\eta'}(k_3) .
\]

Here \(k_1\) denotes the proton momentum in the proton-proton rest frame and \(k_2\) and \(k_3\) are the 3-momenta of η′ and proton in the proton-η′ subsystems. For the estimation of the proton-proton enhancement factor we have used the inverse of the squared Jost function \[22\]. To estimate the model dependence of the result two other extreme solutions for the proton-proton enhancement factor were considered: the Niskanen-Goldberger-Watson parametrization \[23\] and the square of the on-shell amplitude of the proton-proton scattering calculated in the frame of the optical potential with phase shift including strong and Coulomb interactions \[24\].

The proton-proton and η′-proton invariant mass distributions determined for the \(pp \rightarrow pp\eta'\) reaction at an excess energy of \(Q = 16.4\) MeV show an enhancement which may indicate a non negligible P-wave contribution from the proton-proton subsystem \[20, 27\]. Therefore in order to avoid a bias on the result from distortion of higher partial waves we restrict the extraction of the scattering length only to the range \(Q < 11\) MeV. This limitation minimizes also the dependence of the result on the pp-FSI model and reduces the corresponding systematic uncertainty. Moreover the low energy range used in the analysis allowed us to parametrize the η′p FSI enhance-
moment factor with the scattering length approximation

\[ M_{\eta'p} = \frac{1}{1 - ika_{\eta'p}} \]  

(3)

where \( a_{\eta'p} \) is the scattering length of the \( \eta'p \) interaction treated as a free parameter in the analysis.

To determine \( a_{\eta'p} \) we have constructed the following Neyman \( \chi^2 \) statistics

\[ \chi^2(\text{Re}(a_{\eta'p}), \text{Im}(a_{\eta'p}), \alpha) = \sum_{i=1}^{17} \left( \frac{\sigma_i^{\text{exp}} - \alpha \sigma_i^{\text{th}}(a_{\eta'p})}{\Delta \sigma_i^{\text{exp}}} \right)^2 \]  

(4)

where \( \sigma_i^{\text{exp}} \) denotes the \( i \)-th experimental total cross section measured with the statistical uncertainty \( \Delta \sigma_i^{\text{exp}} \) and \( \sigma_i^{\text{th}} \) stands for the calculated total cross section normalized with a factor \( \alpha \) which is treated as an additional parameter of the fit. \( \sigma_i^{\text{th}}(a_{\eta'p}) \) was calculated for each excess energy \( Q \) integrating Eq.(1) over the available phase space [28]. The best fit to the experimental data corresponds to

\[ \text{Re}(a_{\eta'p}) = 0.00 \pm 0.43_{\text{stat}} \text{ fm} \quad \text{(syst. error negligible)} \]

\[ \text{Im}(a_{\eta'p}) = 0.37^{+0.02}_{-0.11}_{\text{stat}} +0.35_{\text{syst}} \text{ fm} \]  

(5)

The statistical uncertainties in this case were determined at the 70% confidence level taking into account that we have varied three parameters [29]. The systematic uncertainties due to the parametrization of the proton-proton interaction used in the analysis were estimated as the maximal difference between the result obtained in Eq.(5) and that determined using the two other \( pp \) FSI models. The real part of \( a_{\eta'p} \) the differences obtained by applying different models are negligible.

It is interesting to compare these results with theoretical expectations and with recent studies based on the \( \eta' \)–nucleus optical potential. In the Quark Meson Coupling model (QMC) [30] one calculates the in-medium meson masses and corresponding effective in-medium meson-nucleon scattering lengths through coupling the light quarks in the meson to the scalar isoscalar \( \sigma \) (and also \( \omega \) and \( \rho \)) mean fields in the nucleus. For 20 degrees \( \eta \)–\( \eta' \) mixing angle, QMC predicts the \( \eta' \) mass shift to be -37 MeV at nuclear matter density \( \rho_0 \), corresponding to the real part of the effective \( \eta' \)–nucleon scattering length being 0.5 fm. This mass shift is very similar to the recent determination of the \( \eta' \)–nucleus optical potential by the CBELSA/TAPS collaboration from studies of \( \eta' \) photoproduction from Carbon [31]. The \( \eta' \)–nucleus optical potential \( V_{\text{opt}} = V_{\text{real}} + iW \) deduced from these photoproduction experiments is \( V_{\text{real}}(\rho_0) = -27 \pm 10(\text{stat.}) \pm 10(\text{syst.}) \) MeV which is equal to the meson mass shift in medium and \( W(\rho_0) = -10 \pm 2.5 \) MeV. Larger mass shifts, downwards by up to 80-150 MeV, were found in NJL [32] and linear sigma model calculations [33]. Each of these theoretical models prefers a positive sign for the real part of \( a_{\eta'N} \) in medium. A chiral coupled channels calculation performed with possible scattering lengths with real part between 0 and 1.5 fm is reported in [34]. A free-space scattering length close to zero was found in a coupled channels fit to \( \eta' \) scattering processes [35]. The energy and density dependence of the \( \eta' \)–(and also \( \eta \))–nucleon scattering lengths is a open topic of investigation [36]. If one assumes no density and energy dependence of the \( \eta' \)–nucleon scattering length, then the value obtained in Eq.(5) is consistent with the QMC result [30] and disfavors the expectations in [32, 33].

In summary, the close to threshold excitation function for the \( pp \to pp\eta' \) reaction was determined down to an excess energy of \( Q = 0.76 \) MeV with the precision \( \Delta Q = 0.10 \) MeV improved by more than a factor of five with respect to previous measurements. The achieved resolution enabled the first quantitative extraction of the scattering length for the \( \eta' \)–proton interaction in free space. Most importantly, the extracted value of the real part of the scattering length is found to be independent of the proton-proton FSI model in the close to threshold energy range (up to 11 MeV) used in the fit.

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