Measurements of the groomed and ungroomed jet angularities in pp collisions at $\sqrt{s} = 5.02$ TeV

ALICE Collaboration

Abstract

The jet angularities are a class of jet substructure observables which characterize the angular and momentum distribution of particles within jets. These observables are sensitive to momentum scales ranging from perturbative hard scatterings to nonperturbative fragmentation into final-state hadrons. We report measurements of several groomed and ungroomed jet angularities in pp collisions at $\sqrt{s} = 5.02$ TeV with the ALICE detector. Jets are reconstructed using charged particle tracks at midrapidity ($|\eta| < 0.9$). The anti-$k_T$ algorithm is used with jet resolution parameters $R = 0.2$ and $R = 0.4$ for several transverse momentum $p_T^{\text{jet}}$ intervals in the 20–100 GeV/c range. Using the jet grooming algorithm Soft Drop, the sensitivity to softer, wide-angle processes, as well as the underlying event, can be reduced in a way which is well-controlled in theoretical calculations. We report the ungroomed jet angularities, $\lambda_\alpha$, and groomed jet angularities, $\lambda_\alpha,g$, to investigate the interplay between perturbative and nonperturbative effects at low jet momenta. Various angular exponent parameters $\alpha = 1, 1.5, 2, 3$ are used to systematically vary the sensitivity of the observable to collinear and soft radiation. Results are compared to analytical predictions at next-to-leading-logarithmic accuracy, which provide a generally good description of the data in the perturbative regime but exhibit discrepancies in the nonperturbative regime. Moreover, these measurements serve as a baseline for future ones in heavy-ion collisions by providing new insight into the interplay between perturbative and nonperturbative effects in the angular and momentum substructure of jets. They supply crucial guidance on the selection of jet resolution parameter, jet transverse momentum, and angular scaling variable for jet quenching studies.

*See Appendix B for the list of collaboration members
1 Introduction

In high-energy particle collisions, jet observables are sensitive to a variety of processes in quantum chromodynamics (QCD), from the initial hard (high $Q^2$) parton scattering to a scale evolution culminating in hadronization near $\Lambda_{QCD}$. Jets reconstructed with a radius (resolution) parameter near $R = 1$ and with sufficiently large transverse momentum $p_T^{\text{jet}}$ provide a proxy for the dynamics of the initial hard parton scattering, whereas those reconstructed with smaller $R$ or at lower $p_T^{\text{jet}}$ become sensitive to nonperturbative effects. In this article, jet substructure observables are defined by clustering particles into a jet and then constructing an observable from its constituents to characterize its internal radiation pattern.

Jet substructure techniques have provided one of the key tools to study rare event topologies in pp collisions, for example by tagging boosted objects that decay into jets \[1\]. Moreover, measurements of jet substructure enable stringent tests of perturbative QCD (pQCD) and facilitate studies of nonperturbative effects which are not yet under satisfactory theoretical control \[2\]. Jet substructure observables offer both flexibility and rigor: they can be constructed to be theoretically calculable from first-principles pQCD while simultaneously maintaining sensitivity to jet radiation in specific regions of phase-space. Jet grooming algorithms, such as Soft Drop \[3–5\], can additionally be used to remove soft, wide-angle radiation via well-controlled approaches, reducing nonperturbative effects. This defines two families of jet substructure observables: one that can be constructed from all jet constituents and one based on a subset of jet constituents which remain after grooming procedures.

One such set of observables are the generalized jet angularities \[6, 7\]. Expanding upon the jet girth $g$ (also known as the jet radial moment), the generalized jet angularities form a class of jet substructure observables defined by

$$\lambda_\alpha^\kappa \equiv \sum \frac{z_i^{\kappa} \theta_i^\alpha}{\mathcal{R}_i}, \quad (1)$$

where the sum runs over the jet constituents $i$, and $\kappa$ and $\alpha$ are continuous free parameters.\[1\] The first factor $z_i \equiv p_{T,i}/p_T^{\text{jet}}$ describes the momentum fraction carried by the constituent, and the second factor $\theta_i \equiv \Delta R_i/R$ denotes the separation in rapidity ($y$) and azimuthal angle ($\phi$) of the constituent from the jet axis, where $\Delta R_i \equiv \sqrt{\Delta y_i^2 + \Delta \phi_i^2}$ and $R$ is the jet resolution parameter. The jet angularities are infrared- and collinear- (IRC)-safe for $\kappa = 1$ and $\alpha > 0$ \[8, 9\]. We consider the ungroomed jet angularities, denoted as $\lambda_\alpha$, as well as the groomed jet angularities in which the sum runs only over the constituents of the groomed jet, denoted as $\lambda_{\alpha,g}$. These include the jet girth \[10\], $\lambda_1$, and the jet thrust \[11\], $\lambda_2$, which is related to the jet mass $m_{\text{jet}}$ by $\lambda_2 = (m_{\text{jet}}/p_T^{\text{jet}})^2 + \mathcal{O}(\lambda_2^3)$; $\lambda_2$, however, is more robust against nonperturbative effects than $m_{\text{jet}}$ since it does not depend explicitly on the hadron masses.

The IRC-safe jet angularities offer the possibility to systematically vary the observable definition in a way that is theoretically calculable and therefore provide a rich opportunity to study both perturbative and nonperturbative QCD \[12, 15\]. This article considers jet angularities constructed from charged-particle jets. While charged-particle jets are IRC-unsafe \[16\], comparisons to these theoretical predictions can nonetheless be carried out by following a nonperturbative correction procedure, as outlined in Sec. \[5\].

Jet angularities were recently calculated in pp collisions both in the ungroomed \[9\] and groomed \[17\] cases, as well as for jets produced in association with a Z boson \[18\]. These calculations use all-order resummation of large logarithms up to next-to-leading-logarithmic (NLL') accuracy \[19\]. Measurements of $\lambda_\alpha$ and $\lambda_{\alpha,g}$ will serve to test these analytical predictions, in particular the role of resummation effects and power corrections. Moreover, by measuring multiple values of $\alpha$, one can test the predicted scaling of nonperturbative shape functions that are used to model hadronization, which depend only on a single

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\[1\] The notation $\lambda_\alpha$ is employed to represent the jet angularities instead of the commonly-used notation $\lambda_2$ in order to avoid conflict with the letter $\beta$, which is also used to denote the angular parameter of the Soft Drop grooming algorithm.
Several measurements of jet angularities have been performed in hadronic collisions. The ungroomed jet angularity \( \lambda_1 \) has been measured in pp collisions by the ATLAS, CMS, and ALICE Collaborations [22–24] in addition to \( pp \) collisions by the CDF Collaboration [25]. The ungroomed jet angularity \( \lambda_2 \) has also been measured in pp collisions by the CMS Collaboration [24]. The closely related ungroomed and groomed jet mass have been extensively measured in pp collisions by the ATLAS and CMS Collaborations [23,24,26–35], and the ungroomed mass was also studied in \( pp \) collisions by the CDF Collaboration [25] and in \( p–Pb \) collisions by the ALICE Collaboration [36]. Many of these measurements have focused on using jet substructure for tagging objects at high \( p_T \), rather than for fundamental studies of QCD, and with the exception of the jet mass there have not yet been comparisons of jet angularities to analytical calculations, nor have any such comparisons been made for charged-particle jets. In this article, we perform the first measurements of groomed jet angularities in pp collisions, and a systematic scan of the IRC-safe ungroomed jet angularities. These measurements focus on low to moderate \( p_T \), and small to moderate \( R \). Moreover, the measurements are performed in pp collisions at a center-of-mass energy \( \sqrt{s} = 5.02 \text{ TeV} \), the same center-of-mass energy at which ALICE recorded data in heavy-ion collisions during LHC Run 2, and where no jet angularity measurements have been made.

These measurements serve as a baseline for future measurements of the jet angularities in heavy-ion collisions, in which a deconfined state of strongly-interacting matter is produced [37–40]. Measurements of jets and jet substructure in heavy-ion collisions may provide key insight into the physical properties of this deconfined state [41–43]. The jet angularities are sensitive both to medium-induced broadening as well as jet collimation [44–46]; by systematically varying the weight of collinear radiation, one may be able to efficiently discriminate between jet quenching models. In Pb–Pb collisions, \( \lambda_1 \) has been measured for \( R = 0.2 \) by the ALICE Collaboration [22], and the ungroomed and groomed jet mass have been measured for \( R = 0.4 \) by the ATLAS, CMS, and ALICE Collaborations [30,34,36]. The interpretation of previous measurements is unclear, with strong modification being observed in Pb–Pb collisions compared to pp collisions for the case when \( \alpha = 1 \) and \( R = 0.2 \), but little to no modification seen for the \( R = 0.4 \) jet mass. Future measurements over a range of \( R \) and \( \alpha \) offer a compelling opportunity to disentangle the roles of medium-induced broadening, jet collimation, and medium response in jet evolution. By measuring small to moderate \( R \) jets in pp collisions, which are theoretically challenging and involve significant resummation effects [47], the ability of pQCD to describe the small-radius jets that are measured in heavy-ion collisions can be tested.

This article reports measurements of ungroomed and groomed jet angularities for \( \alpha = 1, 1.5, 2, \) and 3 in pp collisions at \( \sqrt{s} = 5.02 \text{ TeV} \). In addition to the standard jet girth (**\( \alpha = 1 \)**) and jet mass (related to **\( \alpha = 2 \)**) parameters, \( \alpha = 1.5 \) and \( \alpha = 3 \) are included to test the universality of a nonperturbative shape function by varying effects of soft, wide-angle radiation, as discussed below in Sec. 5.1.2 and to serve as a reference for future jet quenching measurements in heavy-ion collisions. Grooming is performed according to the Soft Drop grooming procedure with \( z_{\text{cut}} = 0.2 \) and \( \beta = 0 \) [48]. Charged particle jets were reconstructed at midrapidity using the anti-\( k_T \) algorithm with jet resolution (radius) parameters \( R = 0.2 \) and \( R = 0.4 \) in four equally-sized \( p_T^{\text{ch}} \) intervals from 20 to 100 GeV/c. The results are compared to NLL pQCD predictions, as well as to the PYTHIA8 [49] and Herwig7 [50,51] Monte Carlo generators.

2 Experimental setup and data sets

A description of the ALICE detector and its performance can be found in Refs. [52,53]. The pp data used in this analysis were collected in 2017 during LHC Run 2 at \( \sqrt{s} = 5.02 \text{ TeV} \) [54]. A minimum bias (MB) trigger was used; this requires a coincidence of hits in the V0 scintillator detectors, which provide full azimuthal coverage and cover the pseudorapidity ranges of \( 2.8 < \eta < 5.1 \) and \( -3.7 < \eta < -1.7 \) [55]. The event selection also requires the location of the primary vertex to be within \( \pm 10 \text{ cm} \) from the non-
From only one vertex. Events were acquired at instantaneous luminosities between approximately 10^{30}
and 10^{31}\text{cm}^{-2}\text{s}^{-1}, corresponding to a low level of pileup with approximately 0.004 < \mu < 0.03 events
per bunch crossing. The pp data sample contains 870 million events and corresponds to an integrated
luminosity of 18.0(4) nb^{-1}. Beam-induced background events were removed using two neutron Zero Degree Calorimeters located
at \pm112.5\text{m} along the beam axis from the center of the detector. Events with multiple reconstructed
vertices were rejected, and track quality selection criteria ensured that tracks used in the analysis were
from only one vertex. Events were acquired at instantaneous luminosities between approximately 10^{30}
and 10^{31}\text{cm}^{-2}\text{s}^{-1}, corresponding to a low level of pileup with approximately 0.004 < \mu < 0.03 events
per bunch crossing. The pp data sample contains 870 million events and corresponds to an integrated
luminosity of 18.0(4) nb^{-1} [56].

This analysis uses charged particle tracks reconstructed from clusters in both the Time Projection Chamber
(TPC) and the Inner Tracking System (ITS). Two types of tracks are defined: global tracks and
complementary tracks. Global tracks are required to include at least one hit in the silicon pixel detector
(SPD), comprising the first two layers of the ITS, and to satisfy a number of quality criteria [59],
including having at least 70 out of a maximum of 159 TPC space points and at least 80% of the
gmetrically findable space points in the TPC. Complementary tracks do not contain any hits in the SPD, 
but otherwise satisfy the tracking criteria, and are refit with a constraint to the primary vertex of the
event. Including this second class of tracks ensures approximately uniform azimuthal acceptance, while
preserving similar transverse momentum p_{T} resolution to tracks with SPD hits, as determined from the
fit quality. Tracks with p_{T,\text{track}} > 0.15 GeV/c are accepted over pseudorapidity |\eta| < 0.9 and azimuthal angle 0 < \phi < 2\pi. All tracks are assigned a mass equal to the \pi^{\pm} mass.

The instrumental performance of the ALICE detector and its response to particles is estimated with a
GEANT3 [60] model. The tracking efficiency in pp collisions, as estimated by propagating pp events
from PYTHIA8 Monash 2013 [49] through the ALICE GEANT3 detector simulation, is approximately
67% at p_{T,\text{track}} = 0.15 GeV/c, rises to approximately 84% at p_{T,\text{track}} = 1 GeV/c, and remains above
75% at higher p_{T}. The momentum resolution \sigma(p_{T})/p_{T} is estimated from the covariance matrix of
the track fit and is approximately 1% at p_{T,\text{track}} = 1 GeV/c. This increases with p_{T,\text{track}}, reaching
approximately 4% at p_{T,\text{track}} = 50 GeV/c.

3 Analysis method

3.1 Jet reconstruction

Jets are reconstructed from charged tracks with p_{T} > 150 MeV/c using the FastJet package [61]. The
anti-\kt algorithm is used with the E recombination scheme for resolution parameters R = 0.2 and
0.4 [62]. All reconstructed charged-particle jets in the transverse momentum range 5 < p_{T,\text{ch jet}} < 200
GeV/c are analyzed in order to maximize statistics in the unfolding procedure (described below). Each
jet axis is required to be within the fiducial volume of the TPC, |\eta_{\text{jet}}| < 0.9 – R. Jets containing a track
with p_{T} > 100 GeV/c are removed from the collected data sample, due to limited momentum resolution.
In order to make consistent comparisons between the data and the theoretical calculations, the
background due to the underlying event is not subtracted from the data, and instead the underlying event
(along with other nonperturbative effects) is included in model corrections, as described in Sec. 5.1.

The jet reconstruction performance is studied by comparing jets reconstructed from PYTHIA8-generated
events at “truth level” (before the particles undergo interactions with the detector) to those at “detector
level” (after the ALICE GEANT3 detector simulation). Two collections of jets are constructed: pp
truth level (PYTHIA truth) and pp detector level (PYTHIA with detector simulation). The detector-
level jets are then geometrically matched with truth-level jets within \Delta R < 0.6 R while additionally
requiring that each match be unique. Table I shows approximate values of the mean jet energy scale
shift, \Delta_{\text{EES}} = \left(\frac{p_{T,\text{ch jet}}}{p_{T,\text{det}}} - \frac{p_{T,\text{ch jet}}}{p_{T,\text{truth}}}\right)/\frac{p_{T,\text{ch jet}}}{p_{T,\text{truth}}}, the jet energy resolution, JER = \sigma\left(\frac{p_{T,\text{ch jet}}}{p_{T,\text{det}}}\right)/\frac{p_{T,\text{ch jet}}}{p_{T,\text{truth}}}, and the
jet reconstruction efficiency, \epsilon_{\text{reco}}, for both R = 0.2 and R = 0.4, where p_{T,\text{ch jet}} is the detector-level p_{T,\text{ch jet}},

\epsilon_{\text{reco}}
Table 1: Approximate values characterizing the jet reconstruction performance for $R = 0.2$ and 0.4 in pp collisions. $\Delta_{\text{JES}}$ is the mean jet energy scale shift, JER is the jet energy resolution, and $\varepsilon_{\text{reco}}$ is the reconstruction efficiency.

| $p_T^{\text{ch jet}}$ | $R = 0.2$ | $R = 0.4$ |
|-----------------------|------------|------------|
| $\Delta_{\text{JES}}$ | -12% | -13% |
| JER | 23% | 21% |
| $\varepsilon_{\text{reco}}$ | 94% | 97% |

and $p_T^{\text{ch, jet, truth}}$ is the truth-level $p_T^{\text{ch jet}}$. The jet energy scale shift is a long-tailed asymmetric distribution due to tracking inefficiency [63] with a peak at $p_T^{\text{ch jet, det}} = p_T^{\text{ch jet, truth}}$, and $\Delta_{\text{JES}}$ should be understood only as a rough characterization of this distribution.

The ungroomed jet angularities are reconstructed using all of the charged-particle jet constituents according to Eq. (1). For the groomed jet angularities, Soft Drop grooming [3] is performed, in which the constituents of each jet are reclustered with the Cambridge–Aachen algorithm [64] with resolution according to Eq. (1). For the groomed jet angularities, Soft Drop grooming [3] is performed, in which the constituents of each jet are reclustered with the Cambridge–Aachen algorithm [64] with resolution parameter $R$, forming an angularly-ordered tree data structure. Each node corresponds to a constituent track, and each edge is a branch splitting defined by $z = \frac{p_T^{\text{subleading}}}{p_T^{\text{leading}} + p_T^{\text{subleading}}}$ and $\theta = \frac{\Delta R}{R} = \sqrt{\Delta\phi^2 + \Delta\eta^2}$. The jet tree is then traversed starting from the largest-angle splitting, and the Soft Drop condition, $z > z_{\text{cut}}\theta^\beta$, is recursively evaluated. Here, $z$ is the subleading branch $p_T$ fraction defined above, and $z_{\text{cut}}$ and $\beta$ are tunable, free parameters of the grooming algorithm. For this analysis, $\beta = 0$ is used to maximize the perturbative calculability [17], while $z_{\text{cut}} = 0.2$ is chosen (as opposed to the more common $z_{\text{cut}} = 0.1$) since higher-accuracy branch tagging can be achieved in future heavy-ion collision analyses [48]. If the Soft Drop condition is not satisfied, then the softer subleading branch is discarded and the next splitting in the harder branch is examined in the same way. If, however, the condition is satisfied, then the grooming procedure is concluded, with all remaining constituents defining the groomed jet. The groomed jet angularity is then defined according to Eq. (1) using the groomed jet constituents, but still with the ungroomed $p_T^{\text{ch jet}}$ and ungroomed jet axis to define $\theta$, since the groomed jet observable is a property of the original (ungroomed) jet object. Note that while the ungroomed $p_T^{\text{ch jet}}$ is IRC-safe, the groomed $p_T^{\text{ch jet}}$ is Sudakov safe [65]. If the jet does not contain a splitting that passes the Soft Drop condition, then the groomed jet contains zero constituents (“untagged”) and does not have a defined groomed jet angularity.

3.2 Corrections

The reconstructed $p_T^{\text{ch jet}}$ and $\lambda_{\text{det}}$ differ from their true values due to tracking inefficiency, particle–material interactions, and track $p_T$ resolution. To account for these effects, PYTHIA8 Monash 2013 [49] [66] and the ALICE GEANT3 detector simulation are used to construct a 4D response matrix that describes the detector response mapping of $p_T^{\text{ch jet}}$ and $\lambda_{\text{det}}$, to $p_T^{\text{ch jet, det}}$ and $\lambda_{\text{det, det}}$, where $p_T^{\text{ch jet, det}}$ and $p_T^{\text{ch jet, truth}}$ are as above, and $\lambda_{\text{det, det}}$ and $\lambda_{\text{det, truth}}$ are the analogous detector- and truth-level $\lambda_{\text{det}}$. The truth-level jet was constructed from the charged primary particles of the PYTHIA event, defined as all particles with a mean proper lifetime larger than 1 cm/c, and excluding the decay products of these particles [67].

A 2D unfolding in $p_T^{\text{ch jet}}$ and $\lambda_{\text{det}}$ is then performed using the iterative Bayesian unfolding algorithm [68] [69] implemented in the RooUnfold package [70] to recover the true jet spectrum at the charged-hadron level. This technique utilizes a “prior” distribution (equivalent to the per-bin MC prediction) as a starting point, before iteratively updating the distribution using Bayes’ theorem in conjunction with the calculated response matrix and measured data (see Refs. [68] [69] for details). Since the jet yield in each reported $p_T^{\text{ch jet}}$ interval varies widely, with higher-$p_T^{\text{ch jet}}$ jets being less probable than lower-$p_T^{\text{ch jet}}$ jets, and since the shape and mean value of the jet angularity distributions also changes with $p_T^{\text{ch jet}}$, a separate 2D unfolding for each reported $p_T^{\text{ch jet}}$ bin is performed in order to optimize the observable binning at both
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truth and detector levels, thus ensuring sufficient jet yield is included in the procedure for all distributions while simultaneously maximizing the number of bins for regions of phase space where higher yield is available. The bin migration in all cases is dominated by a strong diagonal mapping in the response matrix coupled with a slight smearing along the $p_{T,\text{truth}}^{\text{ch\ jet}}$ and $\lambda_{\alpha,\text{truth}}$ axes. The smearing in $\lambda_\alpha$ is roughly symmetric about the diagonal, whereas the smearing in $p_{T,\text{truth}}^{\text{ch\ jet}}$ tends to be skewed towards lower values of $p_{T,\text{truth}}^{\text{ch\ jet}}$ due to tracking efficiency effects.

In the groomed case, the number of untagged jets in the unfolding procedure is included as an additional bin adjacent to the lower edge of the $\lambda_\alpha$ distributions. This is done so that the unfolding procedure will correct for detector effects on the groomed jet tagging fraction as well as account for bin migration effects for jets which are groomed away at detector-level but not truth-level, or vice versa.

To validate the performance of the unfolding procedure, a set of refolding and closure tests is performed, in which either the response matrix is multiplied by the unfolded data and compared to the original detector-level spectrum, or in which the shape of the input MC spectrum is modified to account for the fact that the actual distribution may be different than the MC input spectrum. The number of iterations, which sets the strength of regularization, is chosen to be the minimal value such that all unfolding tests succeed. This results in the number of iterations being equal to 3 for all distributions. In all cases, closure is achieved compatible with statistical uncertainties.

The distributions after unfolding are corrected for the kinematic efficiency, defined as the efficiency of reconstructing a truth-level jet at a particular $p_{T,\text{truth}}^{\text{ch\ jet}}$ and $\lambda_{\alpha,\text{truth}}$ value given a reconstructed jet $p_{T,\text{det}}^{\text{ch\ jet}}$ and $\lambda_{\alpha,\text{det}}$ range. Kinematic inefficiency results from effects including smearing from the Soft Drop threshold and $p_T$-smearing of the jet out of the selected $p_{T,\text{det}}^{\text{ch\ jet}}$ range. Any “missed” jets, those jets which exist at truth level but not at detector level, are handled by this kinematic efficiency correction. In this analysis, minimal detector-level cuts are applied, and the kinematic efficiency is therefore greater than 99% in all cases. Since a wide $p_{T,\text{truth}}^{\text{ch\ jet}}$ range is taken, the effect of “fake” jets, those jets which exist at detector level but not truth level, is taken to be negligible.

4 Systematic uncertainties

The systematic uncertainties in the unfolded results arise from uncertainties in the tracking efficiency and unfolding procedure, as well as the model-dependence of the response matrix, and the track mass assumption. Table 2 summarizes the systematic uncertainty contributions. Each of these sources of uncertainty dominate in certain regions of the measured observables, with the exception of the track mass assumption which is small in all cases. The total systematic uncertainty is taken as the sum in quadrature of the individual uncertainties described below.

The tracking efficiency uncertainty is estimated to be 4% by varying track selection parameters and the ITS–TPC matching requirement. In order to assign a systematic uncertainty to the nominal result, a response matrix is constructed using the same techniques as for the final result except that an additional 4% of tracks are randomly rejected before the jet finding. This response matrix is then used to unfold the distribution in place of the nominal response matrix, and the result is compared to the default result, with the differences in each bin taken as a symmetric uncertainty. This uncertainty constitutes a smaller effect in the groomed jet angularities, where single-particle jets, being the most sensitive to the tracking efficiency, are groomed away by the Soft Drop condition. The uncertainty on the track momentum resolution is a sub-leading effect to the tracking efficiency and is taken to be negligible.

Several variations of the unfolding procedure are performed in order to estimate the systematic uncertainty arising from the unfolding regularization procedure:

1. The number of iterations was varied by $\pm 2$ and the average difference with respect to the nominal
The total unfolding systematic uncertainty is then the standard deviation of the variations, \( \sqrt{\sum_{i=1}^{N} \sigma_i^2 / N} \), where \( N = 4 \) and \( \sigma_i \) is the systematic uncertainty due to a single variation, since they each comprise independent measurements of the same underlying systematic uncertainty in the regularization.

A systematic uncertainty associated with the model-dependent reliance on the Monte Carlo generator which is used to unfold the spectra is included. We construct a fast simulation to parameterize the tracking efficiency and track \( p_T \) resolution, and build response matrices using PYTHIA8 Monash 2013 and Herwig7 (default tune) as generators. Even though a full detector simulation using PYTHIA8 has also been generated, a fast simulation is used for this purpose so that there is complete parity between the two generators in the calculation of this systematic uncertainty. This fast simulation provides agreement within \( \pm 10\% \) of the full detector simulation for \( R = 0.2 \) jets, with some larger deviations seen in the tails of the jet angularity distributions for \( R = 0.4 \) jets. These two response matrices are then used to unfold the measured data, and the differences between the two unfolded results in each interval are taken as a symmetric uncertainty. This uncertainty is most significant at lower \( p_T^{\text{ch jet}} \).

In order to assess the uncertainty due to the track mass assumption, \( \text{K}^{\pm} \) meson and proton masses are randomly assigned to 13% and 5.5% of tracks, respectively, in both the data and the response matrix. These numbers are chosen from the (approximate) inclusive number of each respective particle measured at midrapidity in pp events by ALICE \([71]\). Neither the measurement inside the jets nor the \( p_T^{\text{ch jet}} \) dependence are considered, so these numbers are taken to constitute a reasonable maximum uncertainty. The bin-by-bin difference of the unfolded result to the nominal result is taken as a symmetric uncertainty.

## 5 Results and discussion

We report the \( \lambda_\alpha \) and \( \lambda_{\alpha,g} \) distributions for \( \alpha = 1, 1.5, 2, \) and 3 in four equally-sized intervals of \( p_T^{\text{ch jet}} \) between 20 and 100 GeV/c. The distributions are reported as differential cross sections:

\[
\frac{1}{\sigma} \frac{d\sigma}{d\lambda_\alpha} = \frac{1}{N_{\text{jets}}} \frac{dN_{\text{jets}}}{d\lambda_\alpha} \quad \text{(ungroomed), or} \quad \frac{1}{\sigma_{\text{inc}}} \frac{d\sigma}{d\lambda_{\alpha,g}} = \frac{1}{N_{\text{jets,inc}}} \frac{dN_{\text{gr jets}}}{d\lambda_{\alpha,g}} \quad \text{(groomed),}
\]

(2)

where \( N_{\text{jets}} \) is the number of jets within a given \( p_T^{\text{ch jet}} \) range and \( \sigma \) is the corresponding cross section. For the groomed case, some jets are removed by the grooming procedure, and therefore two different quantities are defined: \( N_{\text{gr jets}} \), the number of jets which have at least one splitting satisfying the Soft Drop condition, and \( N_{\text{inc jets}} \), the total number of inclusive jets, with both \( N_{\text{gr jets}} \) and \( N_{\text{inc jets}} \) being within the given \( p_T^{\text{ch jet}} \) range. \( \sigma_{\text{inc}} \) is the cross section corresponding to the latter inclusive quantity. For the un-groomed case, \( N_{\text{inc jets}} = N_{\text{jets}} \) and \( \sigma = \sigma_{\text{inc}} \), so the redundant labels are dropped. It is useful to normalize the groomed differential cross section by the number of inclusive jets since the groomed jet angularities
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Table 2: Summary of systematic uncertainties for a representative sample of $\alpha$, $R$, and $p_T^{\text{ch, jet}}$. A moderately high $60 < p_T^{\text{ch, jet}} < 80$ GeV/$c$ with $R = 0.4$ is chosen to show the variation with $\alpha$, and two additional rows show the trends with smaller $p_T^{\text{ch, jet}}$ and $R$.

| $\lambda_\alpha$ | $\alpha$ | $R$ | $p_T^{\text{ch, jet}}$ (GeV/$c$) | Trk. eff. | Unfolding | Generator | Mass hypothesis | Total |
|------------------|---------|-----|---------------------------------|-----------|------------|------------|-----------------|-------|
|                  | 1       | 0.4 | 60–80                           | 1–15%     | 2–7%       | 1–5%       | 0–2%            | 7–16% |
|                  | 2       | 0.4 | 60–80                           | 1–10%     | 1–8%       | 1–5%       | 1–3%            | 4–12% |
|                  | 3       | 0.4 | 60–80                           | 1–10%     | 2–4%       | 1–4%       | 0–4%            | 4–11% |
|                  | 2       | 0.4 | 20–40                           | 1–16%     | 1–4%       | 1–43%      | 0–5%            | 2–44% |
|                  | 2       | 0.2 | 60–80                           | 2–12%     | 2–7%       | 1–9%       | 0–2%            | 3–12% |
| $\lambda_{\alpha, g}$ | 1   | 0.4 | 60–80                           | 1–7%      | 2–8%       | 1–6%       | 0–4%            | 2–13% |
|                  | 2       | 0.4 | 60–80                           | 1–8%      | 2–9%       | 1–5%       | 0–4%            | 3–12% |
|                  | 3       | 0.4 | 60–80                           | 1–6%      | 2–7%       | 1–11%      | 0–7%            | 4–16% |
|                  | 2       | 0.4 | 20–40                           | 1–8%      | 2–5%       | 1–40%      | 0–3%            | 2–42% |
|                  | 2       | 0.2 | 60–80                           | 1–7%      | 1–8%       | 1–12%      | 0–3%            | 1–15% |

are a property of the inclusively-measured jet population and are thus typically normalized as such in theoretical calculations [17].

The ungroomed jet angularity distributions are shown in Fig. 1 and Fig. 2 for $R = 0.4$ and $R = 0.2$, respectively. By the definitions given in Eq. 2, these distributions are all normalized to unity. As $\alpha$ increases, the distributions skew towards small $\lambda_\alpha$, since $\theta_i$ is smaller than unity. For larger $R$, the distributions are narrower than for smaller $R$, as expected due to the collinear nature of jet fragmentation. For small $R$ and low $p_T^{\text{ch, jet}}$, there is a visible peak at $\lambda_\alpha = 0$, which is due to single particle jets. These distributions are compared to PYTHIA8 Monash 2013 [49, 66] and Herwig7 (default tune) [50, 51] from truth-level projections of the respective response matrices, with jet reconstruction assigning tracks the $\pi^{\pm}$ meson mass as in the measured data. These comparisons show deviations up to approximately $+50%$ ($-30\%)$. The largest deviations are for small values of $\lambda_\alpha$, where nonperturbative physics becomes significant (see Sec. 5.1 for discussion).

The groomed jet angularity distributions for $z_{\text{cut}} = 0.2$ and $\beta = 0$ are shown in Fig. 3 for $R = 0.4$ and Fig. 4 for $R = 0.2$. Note that these distributions are shown on a logarithmic scale due to the distributions being more strongly peaked and falling faster with $\lambda_\alpha$ as compared to the ungroomed distributions. The groomed jet angularities have significantly smaller values than the ungroomed jet angularities, due to the removal of soft wide-angle radiation. The fraction of “untagged” jets, those that do not contain a splitting which passes the Soft Drop condition, ranges from 10 to 12%. Unlike the ungroomed jet angularities, which are normalized to unity, the groomed jet angularities are normalized to the Soft Drop tagging fraction. Since the tagging rate is fairly large, the measured distributions are therefore normalized close to unity. PYTHIA and Herwig describe the groomed jet angularities slightly better than the ungroomed jet angularities, with most deviations seen in the ungroomed distributions improving by 10–20% in the groomed case. Comparing to the two MC generators, the data are in slightly better agreement with Herwig7 than with PYTHIA8, especially for $R = 0.4$.

The data cover a wide range of $\alpha$ and multiple $R$ down to low $p_T$, and therefore are subject to varying influence from nonperturbative effects. Accordingly, these data can be used to study nonperturbative effects. The level and location of the disagreements with PYTHIA and Herwig provide further constraints on nonperturbative effects in MC event generators. Moreover, the comparison of the groomed
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Figure 1: Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.4$ to MC predictions using PYTHIA8 and Herwig7, as described in the text. Four equally-sized $p_T^{ch\text{ jet}}$ intervals are shown, with edges ranging between 20 and 100 GeV/c. The distributions are normalized to unity.
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**Figure 2:** Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.2$ to MC predictions using PYTHIA8 and Herwig7, as described in the text. Four equally-sized $p_T^{ch\,jet}$ intervals are shown, with edges ranging between 20 and 100 GeV/c. The distributions are normalized to unity.
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Figure 3: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.4$ to MC predictions using PYTHIA8 and Herwig7, as described in the text. Four equally-sized $p_T^{ch\ jet}$ intervals are shown between 20 and 100 GeV/c. The distributions are normalized to the groomed jet tagging fraction.
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Figure 4: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ to MC predictions using PYTHIA8 and Herwig7, as described in the text. Four equally-sized $p_T^{\text{ch \ jet}}$ intervals are shown between 20 and 100 GeV/c. The distributions are normalized to the groomed jet tagging fraction.
and the ungroomed jet angularities with MC event generators allows direct sensitivity to radiation that was groomed away, which is highly nonperturbative.

5.1 Comparison to analytical calculations

The measured ungroomed and groomed jet angularities are compared with analytical calculations \[9, 17\] which use all-order resummations of large logarithms to next-to-leading logarithmic (NLL') accuracy \[19\]. In particular, the calculations resum logarithms of \(\lambda_\alpha\), \(R\), and \(z_{\text{cut}}\). In the case of the \(\lambda_\alpha\) logarithms, the cumulant of the cross section includes the complete set of terms of form \(\alpha_s^n \ln^k \lambda_\alpha\) for \(k = 2n, 2n-1, \) and \(2n-2\). The calculations are valid up to power corrections in \(\lambda_\alpha\), \(R\), and \(z_{\text{cut}}\), and do not include non-global logarithms \[72\]. These calculations are based on the framework of Soft Collinear Effective Theory (SCET) \[73\], in which the jet cross section is factorized into a “hard function” corresponding to the initial scattering, and a “jet function” corresponding to the fragmentation of a hard-scattered parton into a jet. For the calculation of the jet angularities, the jet function is then further factorized into collinear and soft functions. Systematic uncertainties on the analytical predictions are estimated by systematically varying fifteen combinations of scales that emerge in the calculation.

For the ungroomed jet angularities, the collinear-soft momentum scale for the factorization formalism becomes nonperturbative for \[9\]

\[
\lambda_\alpha \lesssim \frac{\Lambda}{p_T^{\text{ch jet}} R},
\]

where \(\Lambda\) is the energy scale at which \(\alpha_s\) becomes nonperturbative, which is taken to be approximately 1 GeV/c. For the groomed jet angularities with \(\beta = 0\), this soft factorization scale becomes nonperturbative for \[17\]

\[
\lambda_{\alpha.g} \lesssim z_{\text{cut}}^{1-\alpha} \left(\frac{\Lambda}{p_T^{\text{ch jet}} R}\right)^\alpha.
\]

Accordingly, the analytical predictions are expected to describe the data only at sufficiently large \(\lambda_\alpha\), which depends on \(p_T^{\text{ch jet}}\), \(R\), and \(z_{\text{cut}}\). On the other hand, for \(\lambda_\alpha = O(1)\), power corrections in \(\lambda_\alpha\) become important, and are not included in the NLL' calculations. Note that for \(\lambda_{\alpha.g} > z_{\text{cut}}\), the groomed and ungroomed predictions are identical at the parton level.

For values of \(\lambda_\alpha\) that are sufficiently large to be described by SCET, corrections for nonperturbative effects must still be applied in order to compare these parton-level calculations to our charged-hadron-level measurements. These nonperturbative effects include hadronization, the underlying event, and the selection of charged particle jets. Note that track-based observables are IRC-unsafe. In general, nonperturbative track functions can be used to directly compare track-based measurements to analytical calculations \[16, 74, 75\]; however, such an approach has not yet been developed for jet angularities. Two techniques are used, described in the following subsections, to apply the nonperturbative corrections.

5.1.1 MC-based hadronization correction

The first technique relies solely on MC generators to transform the parton-level calculations into the final predictions at the charged-hadron level. Two response matrices are constructed, one using PYTHIA 8.244 and the other using Herwig7, which map the jet angularity distributions from jets reconstructed at the final-state parton level (after the parton shower) to those from jets reconstructed at the charged-hadron level. This is done by requiring a unique geometrical match between the parton and charged-hadron-level jets of \(\Delta R < R/2\). The PYTHIA8 simulation uses the default Monash 2013 tune, which is tuned to both \(e^+e^-\) and \(p\bar{p}\) data \[66\], with the only change being that the minimum shower \(p_T^\text{TimeShower:ptMin}\) is set to 0.2 GeV/c, one half of its default value, in order to better match the NLL' predictions at parton level. Herwig7 is also run with the default tune \[76\]. The response matrix generated with both MC simulations is 4D, mapping \(p_T^{\text{parton jet}}\) and \(\lambda_{\alpha,\text{parton jet}}\) to \(p_T^{\text{ch jet}}\) and \(\lambda_{\alpha,\text{truth}}\).
Since the NLL‘ predictions are generated as normalized distributions, each $p_T^{\text{ch jet}}$ interval is first scaled by a value corresponding to the inclusive $p_T^{\text{jet}}$ cross section, calculated at Next-to-Leading Order (NLO) with NLL resummation of logarithms in the jet radius [77]. The 4D response matrix discussed above is then multiplied by these scaled 2D NLL‘ predictions (in both $p_T^{\text{jet}}$, ranging from 10 to 200 GeV/c, and $\lambda_\alpha$) to obtain the theoretical predictions at charged-hadron level. To propagate the systematic uncertainty on the original NLL‘ calculations, this “folding” procedure is performed individually for each of fifteen scale variations, from which a total systematic uncertainty is constructed from the minimum and maximum variation in each interval. Note that this procedure introduces a model-dependence to the comparison, and in fact significantly reduces the magnitude of the systematic uncertainties compared to the parton level; the repetition of this procedure with both PYTHIA8 and Herwig7 is meant to estimate the size of this model dependence.

Although the perturbative accuracy of the MC generators is not clear, by restricting these comparisons to $p_T^{\text{ch jet}} > 60$ GeV/c, there is adequate matching between the analytical calculations and the MC generators’ final-state parton-level predictions to employ the nonperturbative corrections via this mapping procedure. After the folding step, an additional bin-by-bin correction is applied for multi-parton interactions in the underlying event using the respective event generator. More specifically, a ratio is created between the 2D jet angularity distributions generated with multi-parton interactions on versus off at the charged-hadron level, which is then multiplied bin-by-bin by the folded distributions. In all cases, the corrections performed with PYTHIA and those with Herwig are similar in magnitude, indicating that this correction procedure is reasonable.

Figure 5 shows comparisons of the measured ungroomed jet angularities to the folded theoretical predictions for $60 < p_T^{\text{ch jet}} < 80$ GeV/c, for both $R = 0.2$ (top) and $R = 0.4$ (bottom) and for $\alpha = 1.5$ (left), 2 (middle), and 3 (right). Figure 6 shows the corresponding comparisons for the groomed jet angularities. The comparisons for $80 < p_T^{\text{ch jet}} < 100$ GeV/c are shown in Appendix A. Predictions for the $\alpha = 1$ distributions are not currently available due to enhanced sensitivity to soft-recoil, which requires a different factorization [22].

A dashed vertical line is drawn as a rough estimate for the division of perturbative- and nonperturbative-dominated regions, via Eq. 3 or Eq. 4 with $\Lambda = 1$ GeV/c and the mean $p_T^{\text{ch jet}}$ for each interval. Note that the transition from values of $\lambda_\alpha$ which are dominated by perturbative versus nonperturbative physics is actually smooth, and this vertical line is merely intended as a visual guide. The nonperturbative-dominated region of the jet angularities is denoted as $\lambda_\alpha^{\text{NP}}$.

Since the integral for all of the distributions in Fig. 1 through Fig. 4 is fixed at unity by construction, it is important to note that disagreement in the nonperturbative-dominated region induces disagreement in the perturbative-dominated region. Discrepancy in the nonperturbative region is expected due to the divergence of $\alpha_s$ and the corresponding significance of higher-order terms in the perturbative expansion — and will necessarily induce disagreement in the perturbative-dominated region. Accordingly, for these theoretical comparisons, the distributions are normalized such that the integral above $\lambda_\alpha^{\text{NP}}$ is unity.

### 5.1.2 Shape function based correction

An alternate correction technique is also used, which employs a nonperturbative shape function $F(k)$ [14, 20, 21] to correct for the effects caused by hadronization and the underlying event. The shape function is defined as

$$F(k) = \frac{4k}{\Omega_\alpha} \exp \left( -\frac{2k}{\Omega_\alpha} \right),$$

where $k$ is a momentum scale parameter of the shape function, and $\Omega_\alpha$ is described by a single parameter $\Omega = 6/(1 \text{ GeV/c})$ obeying the scaling relation

$$\Omega_\alpha = \Omega/(\alpha - 1),$$
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Figure 5: Comparison of ungroomed jet angularities $\lambda_{\alpha}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions with MC hadronization corrections in the range $60 < p_{T}^{ch\ \text{jet}} < 80$ GeV/c. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha} > \lambda_{\alpha}^{NP}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
Figure 6: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions with MC hadronization corrections in the range $60 < p_T^{ch\ jet} < 80$ GeV/c. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha,g} > \lambda_{NP}^{\alpha}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
and expected to hold universally for hadronization corrections (but not necessarily for underlying event corrections). To correct the parton-level calculations to the hadron level, this shape function is convolved with the perturbative (parton level) jet angularity distribution via numerical integration over argument $k$

$$\frac{d\sigma}{dp_T^{\text{jet}} d\lambda_\alpha} = \int F(k) \frac{d\sigma_{\text{pert}}}{dp_T^{\text{jet}} d\lambda_\alpha} \left( \lambda_\alpha - \lambda_\alpha^{\text{shift}}(k) \right) dk,$$

(7)

where the shift term $\lambda_\alpha^{\text{shift}}(k)$ is either $[17,21]$

$$\lambda_\alpha^{\text{shift}}(k) = \frac{k}{p_T^{\text{jet}} R} \text{ (ungroomed)}, \quad \text{or} \quad z_{\text{cut}}^{1-\alpha} \left( \frac{k}{p_T^{\text{jet}} R} \right)^\alpha \text{ (groomed, with } \beta = 0).$$

(8)

The limits of the integral are thus given by the values of $k$ for which the argument $(\lambda_\alpha - \lambda_\alpha^{\text{shift}}(k))$ is between 0 and 1. Since the nonperturbative parameter $\Omega$ is not calculable within perturbation theory, four values (0.2, 0.4, 0.8, and 2 GeV/$c$) are chosen to observe the different shifting effects. These distributions are then corrected once more using a similar PYTHIA8 folding procedure as described above to account for the effects of only reconstructing charged-particle jets. This correction is dominated by a shift and smearing along the $p_T^{\text{jet}}$ axis.

The comparisons to the ungroomed predictions are shown in Fig. [7] and the groomed predictions are shown in Fig. [8]. The shape function approach, specifically the scaling given in Eq. [6] is not fully justified in the groomed case [78, 79]; nevertheless, reasonable agreement is observed. Since this shape convolution does not require matching to MC at the parton level, the comparisons are extended to the $40 < p_T^{\text{ch jet}} < 60$ GeV/$c$ interval, but below this the perturbative accuracy of the parton-level predictions is insufficient for rigorous comparisons. The comparisons for $40 < p_T^{\text{ch jet}} < 60$ GeV/$c$ and $80 < p_T^{\text{ch jet}} < 100$ GeV/$c$ are shown in Appendix [A].

5.2 Discussion

The $\lambda_\alpha$ distributions are generally consistent with the calculations within uncertainties when $\lambda_\alpha$ is sufficiently large to be in the pQCD regime. This holds approximately independent of $\alpha$, $R$, and $p_T^{\text{jet}}$, and whether or not the jets are groomed. In some distributions, however, particularly for $R = 0.4$, modest disagreement is observed at large $\lambda_\alpha$. This disagreement cannot be unambiguously associated with a particular value of $\lambda_\alpha$ due to the self-normalization of the observable, but rather demonstrates an overall inconsistency in the shape of the distribution. This disagreement could be caused by the unaccounted power corrections in $\lambda_\alpha$, or other effects — and suggests a need for further theoretical investigation. Nevertheless, the overall agreement with the perturbative calculations is striking, given the low-to-moderate jet $p_T$ and $R$ considered.

For $\alpha = 1.5$, the majority of the distributions can be described perturbatively, as $\lambda_\alpha^{\text{NP}}$ is confined towards the left-hand side of the distributions. As $\alpha$ increases to $\alpha = 3$, the influence of the $\lambda_\alpha^{\text{NP}}$ region grows, and the ungroomed distributions become strongly nonperturbative. Similarly, as $R$ increases from $R = 0.2$ to $R = 0.4$, or as $p_T^{\text{ch jet}}$ increases, the size of the perturbative region increases. In the nonperturbative region $\lambda_\alpha < \lambda_\alpha^{\text{NP}}$, the $\lambda_\alpha$ distributions diverge from the calculations. This is expected, since the perturbative approximations break down for $\lambda_\alpha < \lambda_\alpha^{\text{NP}}$, and neither the MC or shape function corrections are necessarily expected to fully correct for missing physics at higher orders or for nonperturbative coupling. In some distributions, the shape-function-based correction is sometimes able to describe the data partially into the nonperturbative regime for suitable values of $\Omega$.

While the overall level of agreement is comparable in both the ungroomed and groomed cases, grooming widens the pQCD regime, as indicated by the location of the dashed blue line in Figures [5,6]. On the other hand, grooming shifts the distributions themselves to significantly smaller values of $\lambda_\alpha$. Nevertheless, this highlights the potential benefit of grooming in heavy-ion collisions in order to retain a larger degree of perturbative control in addition to controlling effects of the underlying event.
Figure 7: Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions using $F(k)$ convolution in the range $60 < p_T^{\text{ch jet}} < 80 \text{ GeV/c}$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_\alpha > \lambda_\alpha^\text{NP}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
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Figure 8: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions using $F(k)$ convolution in the range $60 < p_T^{\text{ch jet}} < 80$ GeV/$c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha,g} > \lambda_{\alpha,g}^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
The performance of the two nonperturbative correction methods — based entirely on MC generators, or on shape functions — are comparable in the perturbative regime. Comparing different values of $\Omega$ for the ungroomed case, where Eq. [6] is justified, there is in many cases only a small difference between the calculations with $\Omega = 0.2$, 0.4, and 0.8 GeV/$c$. However, for $\alpha = 1.5$ and $\alpha = 2$, larger values of $\Omega$ ($\Omega = 2$ GeV/$c$) appear to have more tension with the data in the perturbative regime than smaller values. For $\alpha = 3$, the perturbative region is too small to make any clear statement. One must bear in mind, however, that $\lambda_{NP}^\alpha$ is only a rough characterization of the regime of validity of the perturbative calculation. Consequently, it is unknown whether this disagreement is due to the value of $\Omega$ or due to the breakdown of the perturbative calculation. For smaller values of $\Omega$ (e.g. $\Omega = 0.2$ or 0.4 GeV/$c$), the predicted scaling of Eq. [6] is consistent with the data. Note that the value of $\Omega$ which describes the data is $\mathcal{O}(1)$ as expected for hadronization corrections. These smaller values contrast with a previous result of $\Omega = 3.5$ GeV/$c$ for the ungroomed mass of $R = 0.4$ jets at $200 < p_T^{\text{jet}} < 300$ GeV/$c$ [80], suggesting that the underlying event contribution to $\Omega$, which is not expected to obey the scaling of Eq. [6], may be modified by jets measured at different $p_T^{\text{jet}}$ or by the choice to reconstruct jets using only charged-particle tracks. No significant $R$-dependence is observed in the scaling behavior in this analysis, suggesting that any scaling-breaking underlying event contributions, when also combined with hadronization corrections, are small for $R = 0.2$ and 0.4.

6 Conclusion

The generalized jet angularities are reported both with and without Soft Drop grooming, $\lambda_{\alpha,g}$ and $\lambda_{\alpha}$, respectively, for charged-particle jets in pp collisions at $\sqrt{s} = 5.02$ TeV with the ALICE detector. This measurement of both the ungroomed and, for the first time, the groomed jet angularities provides constraints on models and captures the interplay between perturbative and nonperturbative effects in QCD. Systematic variations of the contributions from collinear and soft radiation of the shower, captured within a given $R$, are provided by measuring the jet angularities for a selection of $\alpha$ parameters. These results consequently provide rigorous tests of pQCD calculations.

The theoretical predictions at NLL$'$ in SCET show an overall agreement with the data for jets with values of $\lambda_{\alpha}$ in the perturbative regime delimited by a collinear-soft momentum scale in the factorization framework of about 1 GeV/$c$. The calculations, after accounting for nonperturbative effects by two different methods, are compatible within about 20% or better with the data in the perturbative region for all explored values of $R$ and $\alpha$. However, larger deviations of up to about 50% are observed in the tails of some distributions, suggesting a need for further theoretical study. By making comparisons solely in the perturbatively-dominated regime, consistency is seen with a predicted universal scaling of the nonperturbative shape function parameter $\Omega_{\alpha}$ with value $\Omega < 1$. A clear breakdown of the agreement is observed for small $\lambda$, where the perturbative calculation is expected to fail. Such nonperturbative effects include soft splittings and hadronization, and these effects dominate over significant regions of the phase space of moderate and low-energy jets. This is corroborated by the comparison of the measured groomed jet angularities to the equivalent theoretical calculations, which demonstrate a wider range of agreement with the perturbative calculations.

These comparisons provide critical guidance for measurements in high-energy heavy-ion collisions where the internal structure of jets may undergo modifications via scatterings of jet fragments with the hot and dense QCD medium. Our measurements demonstrate that any comparison to pQCD must also consider the regimes of $\lambda_{\alpha}$ and $\lambda_{\alpha,g}$ that are controlled by perturbative processes as opposed to those that are dominated by nonperturbative processes. This provides guidance for the selections of $\alpha$, $R$, and $p_T^{\text{ch, jet}}$, and indicates the importance of capturing the complete spectrum of processes (perturbative and non-perturbative) in theory calculations attempting to explain jet quenching.

These measurements further highlight that disagreement between theoretical predictions and data in the
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nonperturbative regime will necessarily induce disagreement in the perturbative regime, when in fact the perturbative accuracy of predictions should only be scrutinized within the perturbative regime. In practice, these measurements give a clear indication that careful inspection is needed when interpreting measurements of jet substructure based on models of jet quenching in heavy-ion collisions for observables including the jet angularity and the jet mass. Future measurements will benefit from the provided guidance demonstrating not only the agreement of jet angularities with pQCD calculations in the perturbative regime but also on selecting on jet angularity differentially with $\alpha$, $R$, and $p_T^{ch\text{jet}}$ in order to maximize theoretical control and interpretation of the perturbative and nonperturbative regimes of jet substructure observables.

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A Additional figures

Figures A.1 and A.2 show the groomed and ungroomed angularities for $80 < p_T^{\text{ch jet}} < 100$ GeV/$c$ using MC generators to apply hadronization corrections. Figures A.3, A.4 and A.5, A.6 show the groomed and ungroomed angularities using the shape function to apply hadronization corrections, for $40 < p_T^{\text{ch jet}} < 60$ GeV/$c$ and $80 < p_T^{\text{ch jet}} < 100$ GeV/$c$.

\begin{figure}[ht]
\centering
\includegraphics[width=\textwidth]{figA1}
\caption{Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL$'$ predictions with MC hadronization corrections in the range $80 < p_T^{\text{ch jet}} < 100$ GeV/$c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_\alpha > \lambda_\alpha^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.}
\end{figure}
Figure A.2: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL$'$ predictions with MC hadronization corrections in the range $80 < p_T^{\text{ch jet}} < 100 \text{ GeV}/c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha,g} > \lambda_{\alpha,g}^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
Figure A.3: Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL’ predictions using $F(k)$ convolution in the range $40 < p_T^{\text{jet}} < 60 \text{ GeV}/c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_\alpha > \lambda_\alpha^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.

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Figure A.4: Comparison of ungroomed jet angularities $\lambda_\alpha$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions using $F(k)$ convolution in the range $80 < p_T^{\text{ch jet}} < 100$ GeV/$c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_\alpha > \lambda_\alpha^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
Figure A.5: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL' predictions using $F(k)$ convolution in the range $40 < p_T^{\text{ch jet}} < 60 \text{ GeV/c}$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha,g} > \lambda_{\alpha,g}^{\text{NP}}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
Figure A.6: Comparison of groomed jet angularities $\lambda_{\alpha,g}$ in pp collisions for $R = 0.2$ (top) and $R = 0.4$ (bottom) to analytical NLL’ predictions using $F(k)$ convolution in the range $80 < p_T^{\text{ch jet}} < 100 \text{ GeV}/c$. The distributions are normalized such that the integral of the perturbative region defined by $\lambda_{\alpha,g} > \lambda_{\alpha,g}^\text{NP}$ (to the right of the dashed vertical line) is unity. Divided bins are placed into the left (NP) region.
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O.A.M. Saarimaki105, R. Sadek117, S. Sadowsky104, J. Saetre121, K. Šafařík38, S.K. Saha143, S. Saha89, B. Sahoo89, P. Sahoo50, R. Sahoo51, S. Sahoo67, D. Sahu51, P.K. Sahu67, J. Saini143, S. Sakai136, S. Sambhyal104, V. Samsonov10496, D. Sarkar145, N. Sarkar143, P. Sarma143, V.M. Sarti108, M.H.P. Sus148, J. Schambach99121, H.S. Scheid106, C. Schiaua106, R. Schicker107, A. Schmich101, C. Schmidt110, H.R. Schmidt106, M.O. Schmidt135, M. Schmidt106, N.V. Schmidt106, A.R. Schmier133, R. Schottler59, J. Schukraft15, Y. Schutz199, K. Schwarz109, K. Schweda110, G. Scilo26, E. Scomparin19, J.E. Seger15, Y. Sekiguchi135, D. Sekihata135, I. Selyuzhenkov11096, S. Senyukov1139, J.J. Seo96, L. Serebryakov65, L. Šerkšnytė108, A. Sevcenco69, T.J. Shaba74, A. Shabanov65, A. Shabetai117, R. Shahoyan35, W. Shaikh112, A. Shangaraev94, A. Sharma103, H. Sharma120, M. Sharma104, N. Sharma103, S. Sharma104, U. Sharma104, O. Sheibani127, K. Shigaki47, M. Shimomura86, S. Shirinkin95, Q. Shou41, Y. Sibiriak91, S. Siddhanta36, T. Siemiarczuk88, T.F. Silva123, D. Silvermyr83, G. Simonetti35, B. Singh108, R. Singh39, R. Singh104, R. Singh21, V.K. Singh143, V. Singh143, T. Sinha12, B. Sitar13, M. Sitta32, T.B. Skaali20, G. Skorodumov107, M. Slupecki13, N. Smirnov148, R.J.M. Snellings64, C. Sonico114, J. Song127, A. Songmoolnak119, F. Sorame28, S. Sorensen33, I. Sputowska20, J. Stachowiak107, I. Stang69, P.J. Steffanic133, S.F. Stiefelmaier107, D. Stocco117, I. Storehaug20, M.M. Storevedt37, C.P. Stylianidis93, A.A.P. Suaide123, T. Sugiyama74, C. Suire36, A. Tikhonov89, Y. Sibiriak38, Y. Zhang17, V. Vechernin135, D. Varga88, M. Varga-Kofarago89, U. Vértesi147, M. Veltchev84, L. Vilkoviev40, Z. Vilakazi135, O. Villalobos Baillie35, J. Virgili30, V. Vodopyanov75, B. Volke35, M.A. Völkl95, S. Vondracek53, W. Vranjes36, I. Vrček40, T. Vretenar111, K. Vysotskii92, A. Vodopyanov77, B. Volkov86, S. Völkl107, K. Voloshin95, S.A. Voloshin145, G. Volpe34, B. von Haller53, I. Vorobyev108, D. Voscek119, N. Voznik45, J. Vrálková39, B. Wagner32, C. Wang41, D. Wang41, M. Weber116, A. Wegrynensky35, S.C. Wenzel35, J.P. Wessels146, J. Wiechula20, J. Wikne20, G. Wilt89, J. Wilkinson110, G.A. Willems146, B. Windelband107, M. Winn140, W.E. Witt133, J.R. Wright21, W. Wu41, Y. Wu131, R. Xu7, A.K. Yadav143, S. Yalcin79, Y. Yamaguchi47, K. Yamakawa27, Y. Yang23, S. Yano97, Z. Yin17, H. Yokoyama64, I.-K. Yoo17, J.H. Yoon63, S. Yuan21, A. Yuncu107, V. Zaccolato24, A. Zaman14, C. Zampolli135, H.J.C. Zanolfi64, N. Zardoshti35, A. Zarochentsev115, P. Závada68, N. Zavialov111, M. Zhalov101, B. Zhang7, S. Zhang31, X. Zhang7, Y. Zhang131, V. Zherebcevskii115, Y. Zhi11, N. Zhigareva92, D. Zhou7, Y. Zhou92, J. Zhu7110, Y. Zhu7, A. Zichichi20, G. Zinovjev3, N. Zurlo14259

Affiliation notes

1 Deceased
2 Also at: Italian National Agency for New Technologies, Energy and Sustainable Economic Development (ENEA), Bologna, Italy
3 Also at: Dipartimento DET del Politecnico di Torino, Turin, Italy
4 Also at: M.V. Lomonosov Moscow State University, D.V. Skobeltsyn Institute of Nuclear, Physics, Moscow, Russia
5 Also at: Department of Applied Physics, Aligarh Muslim University, Aligarh, India
6 Also at: Institute of Theoretical Physics, University of Wrocław, Poland

Collaboration Institutes

1 A.I. Alikhanyan National Science Laboratory (Yerevan Physics Institute) Foundation, Yerevan, Armenia
2 AGH University of Science and Technology, Cracow, Poland
3 Bogolyubov Institute for Theoretical Physics, National Academy of Sciences of Ukraine, Kiev, Ukraine
4 Bose Institute, Department of Physics and Centre for Astroparticle Physics and Space Science (CAPSS), Kolkata, India
5 Budker Institute for Nuclear Physics, Novosibirsk, Russia
6 California Polytechnic State University, San Luis Obispo, California, United States
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ALICE Collaboration

59 INFN, Sezione di Pavia, Pavia, Italy
60 INFN, Sezione di Roma, Rome, Italy
61 INFN, Sezione di Torino, Turin, Italy
62 INFN, Sezione di Trieste, Trieste, Italy
63 Inha University, Incheon, Republic of Korea
64 Institute for Gravitational and Subatomic Physics (GRASP), Utrecht University/Nikhef, Utrecht, Netherlands
65 Institute for Nuclear Research, Academy of Sciences, Moscow, Russia
66 Institute of Experimental Physics, Slovak Academy of Sciences, Košice, Slovakia
67 Institute of Physics, Homi Bhabha National Institute, Bhubaneswar, India
68 Institute of Physics of the Czech Academy of Sciences, Prague, Czech Republic
69 Institute of Space Science (ISS), Bucharest, Romania
70 Institut für Kernphysik, Johann Wolfgang Goethe-Universität Frankfurt, Frankfurt, Germany
71 Instituto de Ciencias Nucleares, Universidad Nacional Autónoma de México, Mexico City, Mexico
72 Instituto de Física, Universidade Federal do Rio Grande do Sul (UFRGS), Porto Alegre, Brazil
73 Instituto de Física, Universidad Nacional Autónoma de México, Mexico City, Mexico
74 iThemba LABS, National Research Foundation, Somerset West, South Africa
75 Jeonbuk National University, Jeonju, Republic of Korea
76 Johann-Wolfgang-Goethe Universität Frankfurt Institut für Informatik, Fachbereich Informatik und Mathematik, Frankfurt, Germany
77 Joint Institute for Nuclear Research (JINR), Dubna, Russia
78 Korea Institute of Science and Technology Information, Daejeon, Republic of Korea
79 KTO Karatay University, Konya, Turkey
80 Laboratoire de Physique des 2 Infinis, Irène Joliot-Curie, Orsay, France
81 Laboratoire de Physique Subatomique et de Cosmologie, Université Grenoble-Alpes, CNRS-IN2P3, Grenoble, France
82 Lawrence Berkeley National Laboratory, Berkeley, California, United States
83 Lund University Department of Physics, Division of Particle Physics, Lund, Sweden
84 Moscow Institute for Physics and Technology, Moscow, Russia
85 Nagasaki Institute of Applied Science, Nagasaki, Japan
86 Nara Women’s University (NWU), Nara, Japan
87 National and Kapodistrian University of Athens, School of Science, Department of Physics, Athens, Greece
88 National Centre for Nuclear Research, Warsaw, Poland
89 National Institute of Science Education and Research, Homi Bhabha National Institute, Jatni, India
90 National Nuclear Research Center, Warsaw, Poland
91 National Research Center Kurchatov Institute, Moscow, Russia
92 Niels Bohr Institute, University of Copenhagen, Copenhagen, Denmark
93 Nikhef, National institute for subatomic physics, Amsterdam, Netherlands
94 NRC Kurchatov Institute IHEP, Protvino, Russia
95 NRC «Kurchatov»-Institute - ITEP, Moscow, Russia
96 NRNU Moscow Engineering Physics Institute, Moscow, Russia
97 Nuclear Physics Group, STFC Daresbury Laboratory, Daresbury, United Kingdom
98 Nuclear Physics Institute of the Czech Academy of Sciences, Rež u Prahy, Czech Republic
99 Oak Ridge National Laboratory, Oak Ridge, Tennessee, United States
100 Ohio State University, Columbus, Ohio, United States
101 Petersburg Nuclear Physics Institute, Gatchina, Russia
102 Physics department, Faculty of science, University of Zagreb, Zagreb, Croatia
103 Physics Department, Panjab University, Chandigarh, India
104 Physics Department, University of Jammu, Jammu, India
105 Physics Department, University of Rajasthan, Jaipur, India
106 Physikalisches Institut, Eberhard-Karls-Universität Tübingen, Tübingen, Germany
107 Physikalisches Institut, Ruprecht-Karls-Universität Heidelberg, Heidelberg, Germany
108 Physik Department, Technische Universität München, Munich, Germany
109 Politecnico di Bari and Sezione INFN, Bari, Italy
110 Research Division and ExtreMe Matter Institute EMMI, GSI Helmholtzzentrum für Schwerionenforschung GmbH, Darmstadt, Germany
111 Russian Federal Nuclear Center (VNIIEF), Sarov, Russia
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ALICE Collaboration

112 Saha Institute of Nuclear Physics, Homi Bhabha National Institute, Kolkata, India
113 School of Physics and Astronomy, University of Birmingham, Birmingham, United Kingdom
114 Sección Física, Departamento de Ciencias, Pontificia Universidad Católica del Perú, Lima, Peru
115 St. Petersburg State University, St. Petersburg, Russia
116 Stefan Meyer Institut für Subatomare Physik (SMI), Vienna, Austria
117 SUBATECH, IMT Atlantique, Université de Nantes, CNRS-IN2P3, Nantes, France
118 Suranaree University of Technology, Nakhon Ratchasima, Thailand
119 Technical University of Košice, Košice, Slovakia
120 The Henryk Niewodniczanski Institute of Nuclear Physics, Polish Academy of Sciences, Cracow, Poland
121 The University of Texas at Austin, Austin, Texas, United States
122 Universidad Autónoma de Sinaloa, Culiacán, Mexico
123 Universidade de São Paulo (USP), São Paulo, Brazil
124 Universidade Federal do ABC, Santo Andre, Brazil
125 University of Cape Town, Cape Town, South Africa
126 University of Houston, Houston, Texas, United States
127 University of Jyväskylä, Jyväskylä, Finland
128 University of Kansas, Lawrence, Kansas, United States
129 University of Liverpool, Liverpool, United Kingdom
130 University of Science and Technology of China, Hefei, China
131 University of South-Eastern Norway, Tonsberg, Norway
132 University of Tennessee, Knoxville, Tennessee, United States
133 University of the Witwatersrand, Johannesburg, South Africa
134 University of Tokyo, Tokyo, Japan
135 University of Tsukuba, Tsukuba, Japan
136 Université Clermont Auvergne, CNRS/IN2P3, LPC, Clermont-Ferrand, France
137 Université de Lyon, CNRS/IN2P3, Institut de Physique des 2 Infinis de Lyon, Lyon, France
138 Université de Strasbourg, CNRS, IPHC UMR 7178, F-67000 Strasbourg, France, Strasbourg, France
139 Università Paris-Saclay Centre d’Etudes de Saclay (CEA), IRFU, Département de Physique Nucléaire (DPhN), Saclay, France
140 Università degli Studi di Foggia, Foggia, Italy
141 Università di Brescia, Brescia, Italy
142 Variable Energy Cyclotron Centre, Homi Bhabha National Institute, Kolkata, India
143 Warsaw University of Technology, Warsaw, Poland
144 Wayne State University, Detroit, Michigan, United States
145 Westfälische Wilhelms-Universität Münster, Institut für Kernphysik, Münster, Germany
146 Wigner Research Centre for Physics, Budapest, Hungary
147 Yale University, New Haven, Connecticut, United States
148 Yonsei University, Seoul, Republic of Korea