Instability of the sliding Luttinger liquid

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Received 6 January 2018, revised 13 March 2018
Accepted for publication 26 March 2018
Published 16 April 2018

Abstract
We revise a phase diagram for the sliding Luttinger liquid (SLL) of coupled one-dimensional quantum wires packed in two- or three-dimensional arrays in the absence of a magnetic field. We analyse whether physically justifiable (reasonable) inter-wire interactions, i.e. either the screened Coulomb or ‘Coulomb-blockade’ type interactions, stabilise the SLL phase. Calculating the scaling dimensions of the most relevant perturbations (the inter-wire single-particle hybridisation, charge-density wave, and superconducting inter-wire couplings), we find that their combination always destroys the SLL phase for the repulsive intra-wire interaction. However, suppressing the inter-wire tunnelling of repulsive fermions (when the charge-density wave is the only remaining perturbation), one can observe a stability region emerging due to the inter-wire forward scattering interaction.

Keywords: sliding Luttinger liquid, scaling dimension, instability

(Some figures may appear in colour only in the online journal)

1. Introduction
The Luttinger liquid (LL) describes one-dimensional (1D) interacting systems with a linear (or linearised) spectrum [1–3]. The interaction strongly enhances the impact of impurities leading to a zero-temperature metal–insulator transition in the presence of either disorder [4] or even a single impurity [5, 6], both being described by the renormalisation group (RG) approach. Progress in the fabrication of low-dimensional nanostructures based on carbon nanotubes [7–10], semiconductor and metallic nanowires [11, 12], self-assembled DNA scaffolds [13, 14], etc, revived the interest in theoretical studies of the LL superstructures. Theoretically, the most challenging bunch of problems in this field is the crossover from the 1D LL behaviour of an individual metallic wire to a 2D or 3D Fermi liquid (FL) behaviour of ensembles of coupled 1D wires. Such finite systems may support various topological states with gapless modes propagating through the edge wires [15].

The conductivity of multi-channel (quasi-1D) strongly-correlated systems demonstrates power law temperature dependence. It has been experimentally observed in many quasi-1D systems, including carbon nanotubes [16], semiconductor nanowires [17], MoSe nanowires [18], NbSe \(_3\) nanowires [12], gold nanowires [19], polymer fibers [20] and newly discovered NB\(_2\)PdS\(_5\) nanowires [21]. These observations can be explained within a multi-channel LL model that neglects single-particle backscattering and many-particle scattering processes. The single-particle backscattering results from disorder and can be neglected in a clean (ballistic) translation invariant wires whereas many-particle scatterings are inherent in strongly correlated systems. Many-particle processes are typically weaker but they are renormalised by interaction and may become dominant at low temperatures. The fact that they are not observed in some of the experiments cited above can be explained by relatively high temperatures at which the multi-particle processes are still ineffective. High-temperature phases of multi-channel strongly correlated fermionic systems, therefore, are well described by the so-called sliding Luttinger liquid (SLL) [24–28, 30]. Nevertheless, at lower temperatures quasi-1D systems fall into either a superconducting (SC) [21] or charge density wave (CDW) [12] states. It is also known
that the inter-wire electron tunnelling is a relevant perturbation which results in the transition from the LL to FL phase [22, 23]. The aim of this manuscript is to establish whether the LL fixed point remains stable in a phase of the SLL assuming realistic intra- and inter-wire interactions.

In the SLL phase, the canonic phase–density variables $(\varphi_j, \theta_j)$ describing bosonised degrees of freedom in each wire $j$ are invariant under the constant shifts. The phase remains stable as long as three distinct inter-wire processes are all RG irrelevant. Namely, these processes are the single-particle (SP) and the particle-hole inter-wire tunnelling which may result in a transverse CDW, and the two-particle hopping resulting in a SC state. The SP processes become irrelevant when a spin gap appears due to an attraction between opposite spins (the Luther–Emery regime [23, 31, 32]). Then the stability of the SLL fixed point would be ensured if the remaining SC (the Luther-Emery regime [23, 31, 32]). Then the stability of.

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In this paper we study a SLL phase in a system of coupled parallel quantum wires packed in two- and three-dimensional arrays.

2. The model

After the standard bosonisation [23], the density fluctuations and current in the $i$th wire are parameterised in terms of two bosonic fields $\theta_i$ and $\varphi_i$ as $\delta \rho_i = \frac{1}{\hbar} \partial \theta_i$, and $j_i = \frac{1}{\hbar} \partial \varphi_i$. We assume a spin-gapped situation when only charge degrees of freedom should be kept. Introducing the vector notations for the two fields describing a set of $N$ wires,

$$\theta = \{\theta_1, \ldots, \theta_N\},$$

$$\varphi = \{\varphi_1, \ldots, \varphi_N\},$$

one writes the Lagrangian density of the set as

$$\mathcal{L} = \frac{1}{2 \pi} [2 \partial_i \varphi^T \partial_i \theta - \partial_i \theta^T \mathcal{V}_{\theta} \partial_i \theta - \partial_i \varphi \partial^T \mathcal{V}_{\varphi} \partial_i \varphi \partial_i \varphi].$$

Here the matrices $\mathcal{V}_{\theta}$ and $\mathcal{V}_{\varphi}$ are diagonal in the absence of inter-wire interactions, with the elements expressed in terms of the velocity $v$ and the Luttinger parameter $K_i$ in each wire as $\mathcal{V}_{\theta}^{ii} = \delta_{ii} (v_i / K_i)$ and $\mathcal{V}_{\varphi}^{ii} = \delta_{ii} v_i K_i$. Adding the inter-wire interactions makes these matrices non-diagonal,

$$\mathcal{V}_{\theta}^{ij} = \delta_{ij} (v_i / K_i) + U_{\theta}^{ij},$$

$$\mathcal{V}_{\varphi}^{ij} = \delta_{ij} v_i K_i + U_{\varphi}^{ij},$$

where the off-diagonal matrix elements $U_{\theta}^{ij}$ and $U_{\varphi}^{ij}$ describe the density–density and current–current interaction strengths between the $i$th and $j$th wires. In the presence of the inter-wire interaction, the local field correlators with Lagrangian density equation (3) can be written in matrix form as

$$\langle \theta(t) \otimes \theta^T(t') \rangle = -2K \ln(t - t'),$$

$$\langle \varphi(t) \otimes \varphi^T(t') \rangle = -2K^{-1} \ln(t - t'),$$

where the Luttinger matrix $K$ is defined [33–35] by the matrix equation

$$KV_{\theta} K = V_{\varphi},$$

which always has a unique solution for real symmetric and positive definite matrices $V_{\theta}$ and $V_{\varphi}$. The name is justified by the fact that, in the absence of inter-wire interactions, $K = \text{diag}\{K_i\}$, and equation (6) are reduced to the standard single-wire expressions.

3. Perturbations

It is convenient to write operators corresponding to the three inter-wire processes defined in the introduction (CDW originating from Coulomb interaction, and SP/SC tunnelling processes) in terms of the creation and annihilation operators for the left-moving ($\hat{L}_i$ and $\hat{L}_j$) and right-moving ($\hat{R}_i$ and $\hat{R}_j$) particles in the $i$th wire, with $\hat{L}_i \sim e^{i\varphi_i}$ and $\hat{R}_i \sim e^{i\theta_i}$, where the bosonic variables for the left- and right-movers are $\theta_i^{LR} \equiv \varphi_i \pm \theta_i$. Then the matrix elements of the three potentially relevant inter-wire couplings are given by

$$\hat{L}_{ij}^{\text{cdw}} \sim \hat{R}_i^{\dagger} \hat{L}_j \sim \cos[\varphi_i - \varphi_j],$$

$$\hat{L}_{ij}^{\text{sc}} \sim \hat{R}_i^{\dagger} \hat{L}_j \sim \cos[\varphi_i - \varphi_j],$$

$$\hat{L}_{ij}^{\text{sp}} \sim \hat{R}_i^{\dagger} \hat{R}_j \sim e^{i(\theta_i - \theta_j)/2} e^{i(\varphi_i - \varphi_j)/2}. \tag{11}$$

The corresponding scaling dimensions are straightforward to derive using the field correlators equation (equation (6)); the results are expressed in terms of matrix elements of the Luttinger matrix $K$ and its inverse $K^{-1}$:

$$\Delta_{ij}^{\text{cdw}} \equiv \dim \left[ \hat{L}_{ij}^{\text{cdw}} \right] = K_{ii} + K_{jj} - 2K_{ij}, \tag{12}$$

$$\Delta_{ij}^{\text{sc}} \equiv \dim \left[ \hat{L}_{ij}^{\text{sc}} \right] = (K^{-1})_{ii} + (K^{-1})_{jj} - 2(K^{-1})_{ij}. \tag{13}$$
\[ \Delta_{ij}^{\text{sp}} \equiv \dim \left[ L_{ij}^{\text{sp}} \right] = \frac{1}{4} \left[ \Delta_{ij}^{\text{cdw}} + \Delta_{ij}^{\text{sc}} \right]. \] (14)

The stability condition (i.e. the irrelevance of all the three perturbations) for a 1D system is that all the three scaling dimensions are greater than the physical dimension, \( 1 + 1 = 2 \):
\[ \Delta_{ij}^{\text{cdw}} \geq 2, \Delta_{ij}^{\text{sc}} \geq 2, \]
\[ \Delta_{ij}^{\text{cdw}} + \Delta_{ij}^{\text{sc}} \geq 8. \] (16)

The last inequality is potentially most stringent so that the single-particle hybridisation might be dangerous for the stability of the SLL phase even when both CDW and SC processes are irrelevant. Let us stress that, as usual, the most relevant process does not necessarily make the strongest impact on observables. The impact also depends on bare values of the inter-wire couplings omitted in equations (9)–(11). Since both \( L_{ij}^{\text{sp}} \) and \( L_{ij}^{\text{sc}} \) involve tunnelling between the \( i \)th and \( j \)th wires, their bare values can be much smaller than that of \( L_{ij}^{\text{cdw}} \) that involves only virtual processes. However, the bare values are totally irrelevant at \( T = 0 \) so that the results based on the analysis of the RG dimensions should survive at low enough temperatures. In the last section, we will come back to the situation when a direct inter-wire tunnelling is suppressed so that only CDW processes should be taken into account.

### 4. Identical wires

If all the wires are identical and packed into a 2D or 3D array, the labels \( i \) are replaced by lattice vectors \( \mathbf{R} \) where \( \mathbf{R} \subset \mathcal{L} \) and \( \mathcal{L} \) is the 1D or 2D lattice of wires. Assuming the interactions to be translationally invariant \( (V_{ij} \rightarrow V_{\mathbf{R} + \mathbf{R}}) \), equation (8) for the Luttinger matrix takes the following form:
\[ \sum_{\mathbf{R}, \mathbf{R} \subset \mathcal{L}} K_{\mathbf{R} + \mathbf{R}}, V_{\mathbf{R} + \mathbf{R}}^{\phi} V_{\mathbf{R} + \mathbf{R}}^{\psi} = V_{\mathbf{R} + \mathbf{R}}^{\phi} \] (17)
where \( \mathbf{r} \equiv \mathbf{R} - \mathbf{R}' \subset \mathcal{L} \) and lengths are measured in units where the inter-wire distance is put to 1. This equation is solved via the Fourier transform:
\[ K_{\mathbf{r}} = \int \frac{d^2 q}{(2\pi)^2} K_{\mathbf{q}} e^{i q \mathbf{r}}, \quad K_{\mathbf{q}} = \sqrt{\frac{V_{\mathbf{q} + \mathbf{q}}}{V_{\mathbf{q}}}}, \]
\[ V_{\mathbf{q}}^{\phi} = V_{\mathbf{0}}^{\phi} + \sum_{\mathbf{r} \neq \mathbf{0}} U_{\mathbf{r}}^{\phi} e^{-i q \mathbf{r}}. \] (19)

Here and below the momentum integration is carried out over a Brillouin zone. This results in the following expressions for the scaling dimensions for the coupling between wires separated by the lattice vector \( \mathbf{r} \):
\[ \Delta_{ij}^{\text{cdw}} = 2 \int \frac{d^2 q}{(2\pi)^2} K_{\mathbf{q}} \left[ 1 - \cos q \mathbf{r} \right]; \]
\[ \Delta_{ij}^{\text{sc}} = 2 \int \frac{d^2 q}{(2\pi)^2} K_{\mathbf{q}}^{-1} \left[ 1 - \cos q \mathbf{r} \right], \] (21)

\[ \Delta_{ij}^{\text{sp}} = 2 \int \frac{d^2 q}{(2\pi)^2} K_{\mathbf{q}} \left[ 1 - \cos q \mathbf{r} \right]; \]
\[ \Delta_{ij}^{\text{sc}} = 2 \int \frac{d^2 q}{(2\pi)^2} K_{\mathbf{q}}^{-1} \left[ 1 - \cos q \mathbf{r} \right], \] (22)

We have assumed above that the wires are arranged into a simple Bravais lattice. For a non-Bravais lattice, the summation in the matrix equation (equation (17)) should be carried out over all the sites in an elementary cell, with the appropriate changes to the Fourier-transform solution.

### 5. Interactions

In the absence of inter-wire interactions, when \( U = 0 \) in equation (4), the Luttinger matrix is diagonal, with all elements equal to \( K \). Assuming that only the nearest neighbouring wires are coupled for all the three perturbations, the scaling dimensions are reduced to
\[ \Delta_{0}^{\text{cdw}} = 2K, \quad \Delta_{0}^{\text{sc}} = \frac{2}{K}, \quad \Delta_{0}^{\text{sp}} = \frac{1}{2} \left[ K + \frac{1}{K} \right]. \] (23)

Obviously, there is no value of \( K \) for which all the scaling dimensions are above 2 so that the SLL is unstable, at least in the absence of long-range interactions. A weak short-range inter-wire interaction cannot stabilise the SLL phase since it gives only small corrections to the RG dimensions in equation (23) which are never simultaneously close to 2. Let us consider the case of a weakly screened Coulomb interaction, with \( U_{\mathbf{r}}^{\phi} = \alpha_{\mathbf{r}} e^{-\kappa |\mathbf{r}|} / |\mathbf{r}| \) in equation (18) and \( \kappa \ll 1 \). Then, we represent \( V_{\mathbf{q}}^{\phi} \) in equation (18) for 2D and 3D arrays as follows:
\[ V_{\mathbf{q}}^{\phi} = V_{\mathbf{0}}^{\phi} \left[ 1 + \alpha_{\mathbf{q} \neq \mathbf{0}} v_{\mathbf{q}} \right], \]
\[ u_{\mathbf{q}}^{(2D)} = -\ln \left[ 1 - 2\beta \cos q + \beta^2 \right], \quad \beta \equiv e^{-\kappa}, \]
\[ u_{\mathbf{q}}^{(3D)} = \sum_{n \neq 0} \frac{\exp[-\kappa \sqrt{n_1^2 + n_2^2}]}{n_1^2 + n_2^2} e^{-i(q_1n_1 + q_2n_2)}. \] (25)

The Fourier-transform of Luttinger matrix \( K \), equation (18), is expressed via \( u_{\mathbf{q}} \) as
\[ K_{\mathbf{q}} \equiv K Q_{\mathbf{q}}, \]
\[ Q_{\mathbf{q}} = \sqrt{1 + \alpha_{\mathbf{q} \neq 0} u_{\mathbf{q}}} \] (27)

The expression under the square root could become negative for some \( q \) if any of the inter-wire interaction strength, \( \alpha_{\mathbf{r}} \) or \( \alpha_{\mathbf{0}} \), exceeds \( \alpha_{\text{WB}} \equiv (2 \ln(1 + \beta))^{-1} \), the boundary of the Wentzel–Bardeen [36] instability, typical for any multichannel system. The standard LL approach is not valid there so that we assume that both interaction strength are bounded from above. The scaling dimensions for the next-neighbours coupling are then expressed as
\[ \Delta_{ij}^{\text{cdw}} = 2K(Q_{\mathbf{q}}), \quad \Delta_{ij}^{\text{sc}} = 2K^{-1}(Q_{\mathbf{q}}^{-1}), \] (29)
where the angular brackets are defined by
The inter-wire interaction opens up a potential region of stability as, in contrast to the case of isolated channels, the inequalities $\Delta^\text{cdw} > 2$ and $\Delta^\text{sc} > 2$ can be both satisfied provided that $\langle Q_q \rangle^{-1} < K < \langle Q_q \rangle^{-1}$. The third condition of stability, $\Delta^\text{sp} = \frac{1}{2}(\Delta^\text{cdw} + \Delta^\text{sc}) > 2$ is more stringent, as it can be satisfied simultaneously with the two previous ones only if

$$\langle Q_q \rangle^{-1} > 3,$$

and either $\langle Q_q \rangle^{-1} < K < K_+$ or $K_- < K < \langle Q_q \rangle^{-1}$, where $K_+ = 2\langle Q_q \rangle^{-1}[1 \pm (1-\frac{1}{2}\langle Q_q \rangle^{-1}\langle Q_q \rangle^{-1})^2]$. For repulsive fermions, $K < 1$, this can only happen when $\langle Q_q \rangle > 1$. When we study numerically these stability conditions, we find that in for 2D and 3D packing there is no stability region of fermion SLL model.

### 6. ‘Coulomb-blockade’ interaction

Now we consider an ultimate long-range interaction, independent on the inter-wire distance. This model interaction can be used simply to test the extreme case of long-range interaction that allows analytic solution. On the other hand, such a model has a region of applicability in the problems related to interacting Kramers’ doublets in a topological insulator where doublets form a set of ‘channels’ not separated spatially from each other. In this case the interaction matrices (in proper units) have the form:

$$V = (1-\alpha) I + \alpha E \Rightarrow V_{ij} = \delta_{ij} + \alpha [1-\delta_{ij}]$$

where all elements of matrix $E$ are equal to unity. The coefficients $\alpha \rightarrow \alpha_{\theta,\varphi}$ for the two types of interaction in equation (4). All such matrices commute with each other. Thus, the solution of equation (8) for the Luttinger matrix is

$$K = V_{\varphi}^{1/2} V_{\theta}^{-1/2}.$$

Assuming a finite number of wires ($=N$) and noticing that $E^2 = N E$, one expresses $V^{-1}$ and $V^{1/2}$ as

$$V^{-1} = \frac{1}{1-\alpha} \left[ \frac{\alpha}{N\alpha + 1 - \alpha} E \right],$$

$$V^{1/2} = \sqrt{1-\alpha} \left[ \frac{1}{N} \left( \sqrt{1 + \frac{N\alpha}{1-\alpha}} - 1 \right) E \right].$$

Using these expressions one finds, with $c_{\varphi/\theta} = \frac{\alpha_{\varphi/\theta}}{1-\alpha_{\varphi/\theta}}$,

$$K = K \sqrt{\frac{1-\alpha_{\varphi}}{1-\alpha_{\theta}}} \left[ \frac{1}{N} \left( \sqrt{\frac{N\alpha_{\varphi}}{1-\alpha_{\varphi}}} + 1 \right) - 1 \right] E.$$

Here again both interaction strength are bounded from above, $\alpha_{\theta,\varphi} < 1$, by the Wentzel–Bardeen [36] instability. The inverse matrix $K^{-1}$ is obtained by swapping $\theta \leftrightarrow \varphi$. Substituting these expressions into equations (12)–(14), the off-diagonal elements cancel out, and only the diagonal ones contribute to the scaling dimensions:

$$\Delta^\text{cdw} = 2KQ, \quad \Delta^\text{sc} = \frac{2}{KQ}, \quad Q = \sqrt{\frac{1-\alpha_{\varphi}}{1-\alpha_{\theta}}}.$$

Thus, although the long-range (screened) Coulomb interwire interaction tends to stabilise the SLL phase, the infinite-range ‘Coulomb-blockade’ interaction simply renormalises the effective Luttinger parameter ($K \rightarrow QK$) and reproduces the results without inter-wire interactions, equation (23). Therefore, when all three perturbations, CDW, SC and SP, exist, there is no stable SLL-phase (where all the perturbations are irrelevant) for arrays of 1D channels and for all reasonable forms of intra- and inter-wire repulsions.

### 7. Suppressed inter-channel scattering

Here we show that a stable SLL can only be realised in a system without a direct inter-channel tunnelling. This can
happen in a spin-gapped system where the single-particle tunnelling is suppressed or for a sufficiently large inter-wire distance where both single-particle and pair SC tunneling bare values are small and, therefore, can be neglected at not too low temperatures. In the latter case we have to consider, alongside with the (long-range) Coulomb interaction, the CDW perturbation only (the spin degrees of freedom simply double number of ‘channels’, \( N \rightarrow 2N \)). It is reasonable to assume that the current–current inter-wire interaction is much weaker than the density–density one so that we put \( \alpha_{\varphi} = 0 \) in equations (24) and (28). We then find \( \Delta_{\text{cdw}} \), equation (29), numerically and present our results for the 2D array in figure 1. The strength of the inter-wire interaction is bounded, \( |\alpha_{\varphi}| \lesssim \alpha_{\text{WB}} \equiv (2 \ln(1 + \beta))^{-1} \), because above the critical value \( \alpha_{\text{WB}} \) the Wentzel–Bardeen [36] instability occurs and this regime is beyond the applicability of our theory. Within the bounds, one immediately notices a competition between intra- and inter-wire interactions. Figure 1(a) shows that inter-wire interactions provide stability for the SLL phase in the absence of the intra-wire interactions (\( K = 1 \)). The graphs in figures 1(b) and (c) also illustrate that turning on the inter-wire interactions stabilises the SLL phase even for \( K < 1 \). Thus, the SLL phase can be in principle observed in the multi-channel array provided that the inter-wire tunnelling necessary for the SP and SC perturbations is suppressed.

8. Conclusions

After analysing all allowed perturbations (single-particle tunneling and two-particle charge-density wave and Josephson couplings) in a SLL consisting of identical channels/wires with no magnetic field applied, we have shown that no physically reasonable inter-wire interaction can stabilize the model, i.e. support ‘confinement’ of particles and their pairs and the ‘sliding’ phase at the same moment. The situation is qualitatively similar in 2D- and 3D-packed arrays. The only possibility for such a description to be valid at the lowest temperature is the suppression of inter-wire hybridisation that can be achieved when either system is spin-gapped (attraction in the spin sector) or magnetic field is applied.

Acknowledgments

VF and IVY acknowledge the hospitality of the Center for Theoretical Physics of Complex Systems, Daejeon, South Korea, where the main part of this project was performed. IVY’s research was funded by the Leverhulme Trust Research Project Grant RPG-2016-044.

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References

[1] Tomonaga S 1950 Prog. Theor. Phys. 5 544
[2] Luttinger J M 1963 J. Math. Phys. 4 1154
[3] Haldane F D M 1981 J. Phys. C: Solid State Phys. 14 2585
[4] Haldane F D M 1981 Phys. Rev. Lett. 47 1840
[5] Giamarchi T and Schulz H J 1988 Phys. Rev. B 37 325
[6] Kane C L and Fisher M P A 1992 Phys. Rev. Lett. 68 1220
[7] Kane C L and Fisher M P A 1992 Phys. Rev. B 46 15233
[8] Furusaki A and Nagaosa N 1993 Phys. Rev. B 47 4631
[9] Bockrath M et al 2001 Science 291 283
[10] Ishii H et al 2003 Nature 426 540
[11] Mason N, Biercuk M J and Marcus C M 2004 Science 303 655
[12] Melosh N A, Boukai A, Diana F, Gerardot B, Badolato A, Petroff P M and Heath J R 2003 Science 300 112
[13] Slot E, Holst M A, van der Zant H S J and Zaitsev-Zotov S V 2004 Phys. Rev. Lett. 93 176602
[14] Seeman N 2003 Nature 421 427
[15] Zheng J, Birktoft J J, Chen Y, Wang T, Sha R, Constantinnou P E, Ginell S L, Mao C and Seeman N C 2009 Nature 461 74
[16] Neupert T, Chamon C, Mudry C and Thomale R 2014 Phys. Rev. B 90 205101
[17] Bockrath M et al 1999 Nature 397 598
[18] Yao Z, Postma H W C, Balents L and Dekker C 1999 Nature 402 273
[19] Bachtold A et al 2001 Phys. Rev. Lett. 87 166801
[20] Kanda A et al 2004 Phys. Rev. Lett. 92 036801
[21] Kar S et al 2009 ACS Nano 3 207
[22] Zaitsev-Zotov S V et al 2000 J. Phys.: Condens. Matter 12 L303
[23] Venkataraman L, Hong Y S and Kim P 2006 Phys. Rev. Lett. 96 076601
[24] Chandni U et al 2011 ACS Nano 5 8398
[25] Chandni U et al 2013 Adv. Mater. 25 2486
[26] Alefish A N et al 2004 Phys. Rev. Lett. 93 196601
[27] Ning W et al 2014 Appl. Phys. Lett. 105 172603
[28] Wen X G 1990 Phys. Rev. B 42 6623
[29] Giamarchi T 2004 Quantum Physics in One Dimension (London: Clarendon)
[30] Golubović L and Golubovic M 1998 Phys. Rev. Lett. 80 4341
[31] O’Hern C S, Lubensky T C and Toner J 1999 Phys. Rev. Lett. 83 2745
[32] Emery V, Fradkin E, Kivelson S and Lubensky T 2000 Phys. Rev. Lett. 85 2160
[33] Mukhopadhyay R, Kane C L and Lubensky T C 2001 Phys. Rev. B 63 081103
[34] Kane C L, Mukhopadhyay R and Lubensky T C 2002 Phys. Rev. Lett. 88 036401
[35] Mukhopadhyay R, Kane C L and Lubensky T C 2001 Phys. Rev. B 64 045120
[36] Vishwanath A and Carpenter D 2001 Phys. Rev. Lett. 86 676
[37] Luther A and Emery V J 1974 Phys. Rev. Lett. 33 589
[38] Seidel A and Lee D H 2005 Phys. Rev. B 71 076601
[39] Yurkevich I V, Galda A, Yevtushenko O M and Lerner I V 2013 Phys. Rev. Lett. 110 136405
[40] Yurkevich I V 2013 Europhys. Lett. 104 37004
[41] Yurkevich I V 2017 Sci. Rep. 7 3550
[42] Kagalovsky V, Lerner I V and Yurkevich I V 2017 Phys. Rev. B 95 205122
[43] Wentzel G 1951 Phys. Rev. 83 168
[44] Bardeen J 1951 Rev. Mod. Phys. 23 261