Abstract: Fluid microstructure nature has a direct effect on turbulence enhancement or attenuation. Certain classes of fluids, such as polymers, tend to reduce turbulence intensity, while others, like dense suspensions, present the opposite results. In this article, we take into consideration the micropolar class of fluids and investigate turbulence intensity modulation for three different Reynolds numbers, as well as different volume fractions of the micropolar density, in a turbulent channel flow. Our findings support that, for low micropolar volume fractions, turbulence presents a monotonic enhancement as the Reynolds number increases. However, on the other hand, for sufficiently high volume fractions, turbulence intensity drops, along with Reynolds number increment. This result is considered to be due to the effect of the micropolar force term on the flow, suppressing near-wall turbulence and enforcing turbulence activity to move further away from the wall. This is the first time that such an observation is made for the class of micropolar fluid flows, and can further assist our understanding of physical phenomena in the more general non-Newtonian flow regime.

Keywords: computational fluid dynamics (CFD); direct numerical simulation (DNS); non-Newtonian flow; micropolar fluid flow; turbulence; turbulent channel flow

1. Introduction

The turbulence generation mechanism is known to alter depending on the internal microstructure of the fluid flow. As a result, study of non-Newtonian turbulent flows has become of great importance not only from a physical point of view, but due to their many real life applications as well. A well-documented class of such fluid flows is polymer solutions, which have widespread industrial applications, as they tend to reduce drag and effectively pressure loss [1,2]. The first one to report this kind of behavior for polymer additives was Toms [3], while since then numerous studies have explored the effects of polymer fluid flows especially in the turbulent regime, with some recent reviews conducted by Graham [4] and White and Mungal [5]. In the majority of these studies, it has been shown that addition of polymeric particles to a Newtonian fluid flow leads to near-wall turbulence dampening.

Another class of fluid that presents an altered behavior in comparison with the classic turbulent Newtonian flow is that of dense suspensions. In a recent work of Picano et al. [6], it has been shown that the addition of a dispersed phase results in drag increase as well as near-wall turbulence intensification. The increased viscosity caused by dense suspensions leads to higher turbulence interaction as volume fraction increases. Studies of dense suspension fluid flows have also been concentrated at the transitional regime between laminar and turbulent flow, with some very interesting results. An experimental study of Matas, Moris and Guazzelli [7] reported that the transitional Reynolds number presents a non-monotonic behavior for particle laden flow. Depending on the particle phase volume fraction, critical Reynolds number first decreases and then increases, while these results have also been numerically extracted by Yu et al. [8].

Turbulent regime of the aforementioned particle laden flows induces even more complexities than the classic Newtonian one. Different approximations have been selected to
study this area, while many parameters have also been considered towards their influence in the turbulence generation mechanism. The so-called two-way coupling approximation has been used among others by Zhao et al. [9], where it has been proven through numerical simulations that added spherical particles can also lead to drag reduction, a property previously known to be valid only for polymeric or fiber additives. Earlier, Gore and Growe [10] showed that particle diameter of the added phase plays a crucial role to the turbulence attenuation or enhancement of the fluid flow. Thus, it can be easily understood that turbulence modulation by suspensions is far from clear, with the set of parameters that affect the enhancement or attenuation still uncertain.

Micropolar theory, which was originally proposed by Eringen [11], is a generalization of the incompressible Navier–Stokes equation for fluids with internal microstructure, and has been previously reported to successfully describe a wide range of fluids with internal microstructure spanning from dense suspensions to liquid crystals, blood and other polymer-like fluids [11–13]. In addition, micropolar fluid theory is attractive as it includes an asymmetric and coupled stress tensor to describe the flow physics, in an Eulerian frame, with no need to treat a discrete phase.

In this article, the turbulent regime of suspensions is explored by employing the micropolar theory constitutive equations [11]. Three different Reynolds numbers are considered in the low Reynolds turbulent regime, while the ratio of micropolar to total viscosity has been varied as well, where micropolar viscosity is the one of the dispersed phase. Our findings support that both the Reynolds number, as well as the ratio of micropolar to total viscosity, affect turbulence modulation, which seems to alter its behavior for sufficiently high values of these parameters. Previous studies have also reported modulation of the turbulence activity in dilute suspensions [9,10,14,15], although the majority of these studies only considers the effect of particle diameter. They mostly report a turbulence attenuation when the particle diameter is less than the turbulent length scale.

2. Materials and Methods

Governing Equations

Direct numerical simulations (DNS) of a turbulent channel flow with internal microstructure have been performed. The set of equations that has been solved (1) and (2), together with the incompressibility condition, \( \nabla \cdot u = 0 \), has been properly non-dimensionalized as:

\[
\frac{\partial u}{\partial t} + (u \cdot \nabla)u = -\nabla P + \frac{1}{Re} \nabla^2 u + \frac{m}{Re} \nabla \times \omega \\
\frac{JN}{m} \left[ \frac{\partial \omega}{\partial t} + (u \cdot \nabla)\omega \right] = \frac{1}{Re} \nabla^2 \omega + \frac{N}{Re} \nabla \times u - \frac{2N}{Re} \omega
\]

where, \( u \) and \( \omega \) are the linear and angular velocity vectors, respectively, and \( t \) and \( P \) stand for time and pressure, respectively. At Equations (1) and (2) four non-dimensional quantities are recovered, i.e., the modified bulk Reynolds number, \( Re = \rho \frac{U_0^2 \delta}{\mu + \kappa} \), with \( \mu \) being the molecular and \( \kappa \) the micropolar fluid viscosities, the so-called vortex viscosity parameter, \( m = \frac{\kappa}{\mu + \kappa} \), the dimensionless microrotation parameter, \( J = \frac{j}{\pi} \), where \( j \) is the microinertia of the fluid, and the so-called spin gradient viscosity parameter, \( N = \frac{\gamma \delta^2}{\mu} \), where \( \gamma \) is the material coefficient of the fluid [16,17]. The linear and angular velocities, time and pressure at the above equations are made dimensionless by selecting the characteristic quantities \( U_0, \frac{U_0}{\delta}, \frac{\delta}{\mu}, \) and \( \rho \frac{U_0^2}{\delta} \), respectively, where \( U_0 \) is the constant mean velocity, \( 2\delta \) is the height of the channel and \( \rho \) is the density of the fluid, which is considered to be homogenous.

Throughout this study, the spin gradient viscosity and the microrotation parameters are kept constant at \( N = 8.3 \times 10^4 \) and \( J = 10^{-5} \) that are usual magnitudes for biological flows [18], while \( m \) is varied between 0 and 0.9. This choice has been based on the straightforward connection between the linear and angular momentum equations through
Fluids near $m = 0$ behave similar to Newtonian ones, while when $m = 0.9$, a microstructure dominated fluid is considered. Increase of $m$ in the present simulations, under constant bulk Reynolds number, implies simultaneously the reduction of molecular viscosity so that the total viscosity of the fluid remains the same. Bulk Reynolds numbers of 3300, 5600 and 13,800 are considered in the present study.

For the numerical simulations that are presented in this article, the open-source CFD platform OpenFoam has been used. A new in-house micropolar fluid solver that is based on the finite volume method has been implemented in the OpenFoam platform. This solver has already been found to accurately predict the analytical solutions of Couette and Poiseuille flows, as well as blood flow in a vessel under realistic conditions [19]. The numerical schemes that have been selected for the solution of the Equations (1) and (2), are second order accurate for all spatial derivatives. Time advance of the variables has been made possible with a second order accurate implicit backward scheme, while the usual pressure-implicit split-operator (PISO) method is used for coupling of momentum with pressure. The PISO algorithm is well-known for its robustness and accuracy, while it requires less CPU time in transient turbulent flow cases [20,21].

In order to assess the validity of results, our numerical facility has been compared against previous ones in the Newtonian regime ($m = 0$) [22–24] and experimental results of particle-laden flows [25], as shown in Figure 1a, where excellent agreement between present and previous results throughout the turbulent regime occurs. Mean streamwise velocity, $U^+$, as well as wall-normal direction, $y^+$, have been normalized by the shear velocity $u_\tau = \sqrt{\tau_w / \rho}$, where $\tau_w$ is the shear stress and $+$ indicates inner (wall) units.

3. Results and Discussion

In Figure 1a–c, curves of $U^+$ have been plotted along $y^+$ for all three cases of Re, while the viscosity ratio parameter, $m$, has been varied for $m = 0, 0.4$ and 0.9 as well. Results of these cases present a particular interest, as two different trends can be detected. The first one concerns the comparison of cases with the same Re and different viscosity ratio $m$. By closely examining the results presented in Figure 1a–c, it is understood that the normalized streamwise velocity, $U^+$, collapses to lower values as $m$ increases, indicating higher turbulence activity. This observation holds true, according to the present results,
for all three Re. In the latter case of constant viscosity ratio \( m \) and different Re, a peculiar behavior can be observed. When viscosity ratio \( m = 0 \), curves of \( U^+ \) collapse again to lower values as Re increases, as anticipated. On the opposite side, though, for higher values of \( m \) and more specifically when \( m = 0.9 \), curves of \( U^+ \) present a non-monotonic behavior, where they collapse to lower values as Re increases from Re = 3300 to Re = 5600 and then to higher ones for Re = 13,800, indicating turbulence attenuation.

The behavior that has been described above is similar to turbulence attenuation phenomena observed by Zhao et al. [9], where higher \( U^+ \) profiles have been observed for the particle-laden channel flow case, compared to the unladen case, at approximately similar Re. In their case though, this was achieved by selecting appropriately small particles, which resulted in drag reduction. The departure, due to internal microstructure, of the drag mechanism is also explored in this study, through the percentage of drag increase or reduction, which is defined as:

\[
D = -\frac{d\langle p \rangle}{dx} - \left( -\frac{d\langle p \rangle}{dx}\right)_{0} \times 100\% = \frac{u_T^2 - u_{T0}^2}{u_{T0}^2} \times 100\% \quad (3)
\]

Variables in Equation (3) with subscript 0 refer to Newtonian values, while those without to micropolar. The strategy of analysis has been kept the same as in previous studies of non-Newtonian and polymer flows [2], by plotting results in terms of their drag increase percentage, in Figure 2, where two different trends can be detected depending on Re and viscosity ratio \( m \).

![Figure 2. Drag increase percentage values (D%) for: Re = 3300, 5600 and 13,800 of the present: m = 0, 0.1, 0.4 and 0.9 cases.](image)

For a relatively low values of viscosity ratio, \( m = 0.1 \), drag increase percentage reaches higher values as Re increases, a behavior similar to the Newtonian one. On the other hand, for a higher viscosity ratio, \( m = 0.9 \), the percentage of drag increase drops for higher Re. Even for this case though, there is no drag reduction as compared to the Newtonian case. Still, a reverse behavior exists in comparison with lower Re of same viscosity ratio, which would probably lead to even lower values of drag increment as Re increases. There seems to exist a certain threshold, connected with a combination of \( m \) and Re, above which no further drag increase is possible. In-between values of \( m = 0.4 \) and \( m = 0.7 \), present a rather unstable behavior (more evident in the \( m = 0.7 \) case), which probably marks the transition to the behavior that has been described before.

Findings in terms of drag modulation presented in Figure 2, are in alignment with those that have been found above in Figure 1. In similar reports of fluid flows with internal microstructure [26], drag and turbulence modulation have been connected to the solid-phase contribution to production and dissipation of turbulent kinetic energy (TKE)
of the fluid phase. In this context, the investigation of the present model’s TKE budget is appropriate in order to further explain the observed behavior. The equation for the plane-averaged turbulence kinetic energy is $\langle q \rangle = \langle u_i u_i \rangle$, and the budget may be written as:

$$\frac{D \langle q \rangle}{Dt} = P_{ii} + T_{ii} + D_{ii} + \Pi_{ii} + l_{ii} - \epsilon_{ii}$$  \hspace{1cm} (4)

The terms of Equation (4) are, respectively, the production of kinetic energy due to velocity gradient, transport of kinetic energy by the turbulent velocity fluctuations, the viscous diffusion rate, the transport by pressure fluctuations, production of kinetic energy due to micropolar velocity and the dissipation rate. We choose to focus on these terms that are directly connected to turbulence production or dissipation of the fluid flow. Usually, the main term that enhances turbulence is the production term calculated as:

$$P_{ii} = -u_i u_j \frac{\partial U_i}{\partial x_j}$$  \hspace{1cm} (5)

Previous studies [27] in the Newtonian turbulent regime have shown that as Re increases, turbulence increases as well, through enhancement of the production term. The same also holds true for the dissipation term in Equation (6), which is responsible for loss of kinetic energy:

$$\epsilon_{ii} = \frac{1}{Re} \left( \frac{\partial u_j}{\partial x_j} \frac{\partial u_i}{\partial x_i} \right)$$  \hspace{1cm} (6)

In the present case, as micropolar effects and Re increase, turbulence presents a non-monotonic behavior. Once again, energy loss through the dissipation term reaches higher values for the cases of higher turbulence. In contrast with what has been described above for Newtonian flows, the kinetic energy production term drops as $m$ increases, a fact which indicates that an additional turbulence production mechanism should be present. This term comes from the micropolar velocity contribution to the turbulent kinetic energy balance and is given by:

$$l_{ii} = \frac{m}{Re} (\nabla \times \omega_i) u_j$$  \hspace{1cm} (7)

In order to present a better visualization of the Re and viscosity parameter effect on turbulence production, normalized micropolar ($l_{ii}$) and velocity gradient production ($P_{ii}$) terms have been integrated from 0 to $h$, and results are presented in Figure 3. Interestingly here it can be observed, that for both cases of micropolar viscosity, the integral of the velocity gradient production term drops to lower values as Re increases. On the other hand, the behavior of the micropolar production term integral varies for the different cases of $m$. More specifically, for the lower case of $m = 0.2$, there is almost no noticeable change as Re increases, while there is a sharp drop for the case of $m = 0.9$. Here lies the probable explanation of the behavior previously described in this letter. The micropolar production term provides the ability to the flow, to sustain higher turbulence and drag, this is also the reason why, compared to the Newtonian case, all micropolar cases present enhanced turbulence and drag. The attenuation of the micropolar production though, for the case of $m = 0.9$ as Re increases, forces the normalized velocity profile to collapse to higher values as presented in Figure 1.

The observation above is further enhanced by examining results of the normalized micropolar velocity, $\omega_i^+$, which has been plotted in Figure 4 along $y^+$ for various $m$ and Re. In order to keep the results presentation comprehensible, only two values of Re have been selected to be presented here ($Re = 3300, 13,800$), along with three different values of the viscosity parameter ($m = 0.2, 0.4 \text{ and } 0.9$). Mean value of micropolar velocity survives only in the spanwise direction and is of the same nature as vorticity, but in an active way representing an additional force acting on the flow. The fact that for higher Re, normalized micropolar velocity drops to lower values, while at the same time moves away from the
wall, not only enhances our previous findings, but also adds more information. Essentially, this leads to the conclusion that the additional micropolar force suppresses near-wall turbulence and leads turbulent activity away from the wall.

Figure 3. Integral values (S) of: (■) Velocity gradient production term, (▲) micropolar production term; (red line) $m = 0.2$, (blue line) $m = 0.9$ plotted along $Re = 3300, 5600$ and $13,800$.

Figure 4. Normalized spanwise micropolar velocity ($\omega^\pm_z$) for: $Re = 3300$ and $5600$ of the present: $m = 0.2, 0.4$ and $0.9$ cases.

Finally, in order to have a better visualization of the physical phenomena that have been described above, 2D snapshots of the streamwise Newtonian and spanwise micropolar velocity have been plotted in Figures 5 and 6. In Figure 5, the flow field reveals greater turbulence intensity as $Re$ and viscosity parameter $m$ increase, while turbulent phenomena become more intense closer to the wall. Furthermore, in Figure 6 for cases of higher $Re$ and viscosity ratio $m$, micropolar velocity develops a thinner layer closer to the wall in contrast to the cases of lower $Re, m$. This observation confirms our previous claims that the additional micropolar force term suppresses near-wall turbulence and enforces the departure of turbulent activity from the walls.
Figure 5. Fluid flow snapshots of streamwise velocity via 2D graphs in the $Z - Y$ plane, from top to bottom: $m = 0, Re = 3300; m = 0.9, Re = 3300; m = 0, Re = 13,800$ and $m = 0.9, Re = 13,800$. Contour levels: 0; 0.1; 1.

Figure 6. Fluid flow snapshots of streamwise micropolar velocity via 2D graphs in the $Z - Y$ plane, from top to bottom: $m = 0, Re = 3300; m = 0.9, Re = 3300; m = 0, Re = 13,800$ and $m = 0.9, Re = 13,800$. Contour levels: $-6; 1; 6$.

4. Conclusions

Summarizing, the micropolar fluid model has been employed in order to explore the turbulent regime, as well as turbulence modulation, of channel fluid flows with internal microstructure. Direct numerical simulations have been used for the computational experiments, while constants and material parameters have been based on biological flow values in order to obtain more realistic results [18]. Three different bulk Reynolds numbers have been selected in order to explore the turbulent regime $Re = 3300, 5600, 138,800$, while the micropolar parameter $m$ has been given values from 0 to 0.9, and the rest of the parameters have been kept constant. The selection to vary only $m$ was based on the direct impact that this parameter has on the flow field equations.
Present study results have been compared against previous well established turbulent flow cases [22–25] and presented excellent agreement. In addition, they revealed a non-monotonic behavior of turbulence and drag depending on the viscosity ratio parameter $m$ and $Re$. Thus, for sufficiently high values of $m$ and $Re$, energy production due to the micropolar effect drops to lower values indicating lower turbulence intensity. Results have been further supported by the normalized mean micropolar velocity plot, where curves of higher $Re$ collapse to lower values while they also move further away from the wall, indicating that near-wall turbulence is suppressed by the activity of the additional micropolar force term for high $Re$. Finally, 2D contours of the Newtonian and micropolar velocities have been presented, where the flow physics described above could be better visualized.

The present study reveals for the first time the turbulence modulation of a micropolar fluid flow, considering three different $Re$. The flow physics phenomena that have been revealed present a particular interest not only for the micropolar class of fluids, but also for the more general non-Newtonian flow field, where their behavior in the turbulent regime remains still not fully described. Thus, for the reasons stated above, this study is ranked among pioneer ones.

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