Characterization of floc structure and strength: Role of changing shear rates under various coagulation mechanisms

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1. Introduction

Coagulation and flocculation, based on hydrolyzing metal salts, are widely applied processes to remove suspended colloid particles and natural organic matter in water and wastewater treatment. There are mainly two mechanisms in the metal salts coagulation, i.e., charge neutralization and sweep flocculation [1]. Generally, the effectiveness of flocculation is measured by the parameters such as residual turbidity or DOC removal because they are directly related to the solid–liquid separation and water quality. However, they provide only limited information on the flocculation process. The information of floc size distribution and structure would be much expected [2].

The steady-state floc size distribution is influenced by the balance between rate of aggregation and breakage [3–5]. The physicochemical and hydrodynamic conditions play significant roles simultaneously. The evolution of floc size distribution during flocculation is accompanied by the change of floc structure. The fractal structure of flocs had been observed, measured and analyzed by experimental, numerical simulation or theoretical methods [6–18]. However, from numerical simulation and theoretical perspectives, available researches focused mainly on the computer simulation, geometry analysis and material conservation [15–20].

For example, according to the concept of diffusion-limited aggregation (DLA) and other theoretical analysis, there are several active sites on the surface of fractal aggregates [16–18]. The evolution of fractal structure with continuously changing of shear condition and the mechanism involved have not been given sufficient attention [15].

Floc strength is another particularly important characteristic and plays a significant role in the effectiveness of water treatment plants. Water treatment processes are often non-ideal with many possible zones of higher shear forces that will induce breakup of floc. Flocs must resist these stresses to prevent being broken into smaller clusters because, in practical sense, small clusters generally have lower removal efficiencies. Generally, floc strength is considered to be dependent on the bonding of colloid particles in the aggregates [4,21–23]. As an assumption, the compactness of flocs is positively related to floc strength, however, there is no reasonable mechanic method to evaluate this relationship. Floc strength is directly related to floc structure and is, therefore, highly dependent on the floc formation process. Fractal dimension is characterized as an essential parameter to describe the floc structure and influenced comprehensively by the physicochemical and hydrodynamic conditions such as pH value, shear conditions, and types of coagulants and colloid particles [24–28].

In order to investigate the evolution of fractal structure and strength of flocs, a new method to calculate the strength of flocs was introduced and the calculation results were compared with the results of strength factor determined by small angle
laser light scattering technology. Based on the concept of RLCCA (reaction limited cluster–cluster aggregation) and DLCCA (diffusion limited cluster–cluster aggregation) model, fractal dimensions of flocs formed in different shear conditions and coagulation mechanics were analyzed. The mechanism of restructure was also discussed. Finally, the relationship between fractal dimension and floc strength was discussed using the new method.

2. Method development

Two fundamental approaches have been taken in measuring floc strength [4]. One is the macroscopic measurement and the other is microscopic measurement. The macroscopic measurement is more often be utilized and focused on the energy required in a system for floc breakage. Meanwhile, some useful parameters such as floc strength factor and FI index were induced [13, 24, 25]. Strength factor and recovery factor can be defined as [13]:

\[
\text{strength factor} = \frac{d(2)}{d(1)} \times 100 \quad (1)
\]

\[
\text{recovery factor} = \frac{d(3) - d(2)}{d(1) - d(2)} \times 100 \quad (2)
\]

\(d(1)\) and \(d(3)\) represents the stable floc size before and after breakage, while \(d(2)\) represents the floc size during breakage.

Jarvis et al. [13] investigated strength of NOM flocs coagulated with different coagulants by small angle laser light scattering technology and concluded that the strength of flocs is in the order: PDAMDAC flocs > ferric flocs > alum flocs. Gregory [25] used photometric dispersion analyzer to study the breakage and recovery behaviors of kaolin particles and found that the reversibility of PDAMDAC flocs were better than alum flocs. Previously, Meakin [29] concluded that the fractal dimension was related with the population and mass of flocs by:

\[
N_f = \left( \frac{d_f}{d_0} \right)^{D_F} \quad (3)
\]

\[
M_f = \frac{\pi}{6} d_0^3 d_f^{D_F} \quad (4)
\]

Because of the volume of flocs was calculated by \(V_f = \pi/6 d_f^3\), the compactness of flocs can be expressed as:

\[
\lambda = \frac{(\pi/6) d_f^3 N_f}{(\pi/6) d_0^3} = \left( \frac{d_f}{d_0} \right)^{D_F-3} \quad (5)
\]

Thus, the porosity of flocs can be determined by:

\[
\varepsilon = 1 - \lambda = 1 - \left( \frac{d_f}{d_0} \right)^{D_F-3} \quad (6)
\]

Taking account of the study by Tang et al. [30], strength of fractal aggregates is calculated by:

\[
\sigma_T = \frac{1 - \varepsilon}{\varepsilon} \frac{F}{d_0^2} \quad (7)
\]

\(\sigma_T, \varepsilon\) and \(d_0\) represent the tensile strength of aggregates, the bonding forces between primary particles, the porosity of aggregates and the diameter of primary particles, respectively. In addition, the Bingham critical shear stress, which has a tight relationship with the concentration of particles and the fractal dimension, provides a fine estimation to the floc strength based on the concept of self-similar floc structure [31–33]:

\[
\tau_B \propto \psi^{2/(3-D_F)} \quad (8)
\]

If considering the flocs as sphere and using \(\tau_B\) to replace \(\sigma_T\), Eq. (7) can be equivalently written as:

\[
\tau_B = \frac{1 - \varepsilon}{\varepsilon} \frac{F}{d_0^2} \quad (9)
\]

Based on the Eq. (6), Eq. (9) can be replaced by:

\[
\tau_B = \frac{1}{1 - \left( \frac{d_f}{d_0} \right)^{3-D_F}} \left( \frac{F}{d_0^2} \right) \quad (10)
\]

Finally, the strength of flocs can be calculated by Eq. (10).

3. Materials and methods

3.1. Suspension preparation and coagulant

Kaolin was used as primary particles in this experiment and the solid concentration of suspension was 137 g/L determined by gravimetry. During the high-shear condition, 300 g of kaolin was dispersed in 1000 ml of deionized water. After 30-min mixing, the pH of suspension was adjusted to 7.50 ± 0.05 (MP220, Mettler-Toledo, Switzerland) by adding 0.1 mol/L NaOH and the blending suspension was settled for 24 h in a measuring cylinder. Then the top suspension was decanted into another container as the model suspension. The average size of the particles in suspension was closed to 4 μm, measured by laser light scattering (Mastersizer 2000, Malvern, UK).

The kaolin concentration of 50 mg/L was prepared by diluting the stock suspension with tap water. In addition, a small amount of humic acid was added into the raw suspensions in order to avoid the disturbance of Ca²⁺ and Mg²⁺ in tap water [25]. The pH value of raw suspension was 7.68 ± 0.10 and the suspensions used in experiment was adjusted to 7.50 ± 0.05 by adding 0.1 mol/L HCl. All of the experiments were preceded in room-temperature (23 ± 2°C) and repeated three times.

Alum (Al₂(SO₄)₃·18H₂O, analytic reagent) was used as coagulant to form colloid aggregates. Stock alum solutions were prepared as 0.1 M solution in deionized water.

3.2. Floc structure analysis

The experiment was conducted in 1-L beaker with 800 ml diluted kaolin suspension. The rotary speeds and the stirring times of the impellers can be pre-set.

Fractal dimension of colloid aggregates was measured by light scattering [34]. The light intensity scattered by particles, is proportional to the particles size. Small particles scatter light at high angles, while large particles scatter at lower angles. In light scattering study, the scattered intensity as a function of the magnitude of the scattering wave vector, \(Q\), is measured, where,

\[
Q = \frac{4\pi\sin(\theta/2)}{\lambda} \quad (11)
\]
Table 1

| Experiment mode | Description |
|-----------------|-------------|
| 40 + 60 (gradually increased shear) | 40 rpm (5 min) + 45 rpm (5 min) + 50 rpm (5 min) + 55 rpm (5 min) + 60 rpm (5 min) + 400 rpm (2 min) + 40 rpm (20 min) |
| 60 + 40 (gradually decreased shear) | 60 rpm (5 min) + 55 rpm (5 min) + 50 rpm (5 min) + 45 rpm (5 min) + 40 rpm (5 min) + 400 rpm (2 min) + 40 rpm (20 min) |
| 40 (stable 40 rpm shear) | 40 rpm (25 min) + 400 rpm (2 min) + 40 rpm (20 min) |
| 60 (stable 60 rpm shear) | 60 rpm (25 min) + 400 rpm (2 min) + 40 rpm (20 min) |

Dynamic aggregate size during growth and breakage was measured by laser scattering (Mastersizer 2000) when the jar test was proceeding. The suspension was monitored by drawing water through the optical unit of the Mastersizer and put back into the beaker by a peristaltic pump through plastic tubing with 5 mm inner diameter. In addition, the flow rate of pump was 25 ml/min in order to prevent the flocs from further aggregating or breakup. The pump was located downstream of the Mastersizer to avoid the effects of possible aggregates breakage in the pinch portion of pump. Moreover, size distributions were measured every 40 s taking into account of the duration of jar test.

4. Results and discussion

4.1. Fractal dimension

Fig. 2 shows the fractal dimension of flocs in the first controlled experiments. It was obviously that the fractal dimension of flocs increased as the flocs formation with different shear conditions adopted. The steady-state floc size distribution is a dynamic balance between aggregation and breakage [4] as aggregation and breakup always happen together with the growth of flocs. At the beginning of experiment, primary particles rapidly aggregate as the result of shear condition, simultaneously, some pores are formed in the inner of flocs. With the growth of flocs, cluster–cluster aggregation gradually plays an important role in the development of flocs. Some small but compact clusters will then have chance to penetrate into the inner pores of large flocs. As a result, the fractal dimension will be increased as the growth of flocs. It is easily understood that the higher the shear rate is, the more breaking possibility large flocs have. Thus, flocs formed in higher shear rate will have larger fractal dimension. Furthermore, it seems that flocs are sensitive to the change of shear conditions. Therefore, flocs formed in the “40 + 60” conditions are more feasible to be broken and result in the highest fractal dimension by the floc re-structure as the shear rate gradually increasing.

It is generally considered that fractal structure will not be affected by breakage because the self-similarity of aggregates [10,12,29], but this is not suitable for the flocs formed by electrostatic force. As shown in Fig. 2, there is some, even great, distinction of fractal dimensions after breakage, as considering the charge neutralization and sweeping flocs.

A possible explanation for these inconsistencies is that, although fractal structure or self-similarity is generally inspected in colloidal system [29], strictly self-similar structure is only an ideal concept and practical flocs are considered to have two or more characteristic fractal dimensions as a result of multilevel structure or multi-fractal characteristics [13,36]. Furthermore, self-similar fractal structure hardly relates to exterior conditions and evolution progress of floc growth.

Obviously, fractal dimension will be varied as exterior conditions such as the residual coagulant and primary particles have changed after breakage. Based on the DLA model and other available theoretical studies, growth of flocs always occurs in active sites. As a result, the size of flocs will achieve the balance with the shear condition although there are a large number of pores in the inner of flocs. Nevertheless, these pores have not achieved...
adsorption saturation and have the ability to combine with other particles or clusters further. Flocs which have achieved the size balance may have potential to make them more compact and finally improve the floc strength. In “40 + 60” conditions, the shear rate gradually increases from 40 rpm to 60 rpm, some of the surface bonds are more possible to be properly destroyed than other conditions because flocs are sensitive to the change of shear rate [37]. As a result, some inner parts of flocs are exposed and filled by particles or clusters. Consequently, these flocs are more compact than clusters formed in stable shear rate conditions. Since floc structure is influenced by floc history, fractal dimension of flocs in “40 + 60” is higher than those of “60 + 40” and “40” flocs. Moreover, this explanation may provide another possible mechanism on floc history. Meanwhile, this is the reason why one of the experiments is designed as the gradually increased shear rate.

During the breakage stage, fractal dimensions of flocs are higher than the fractal dimension of flocs before breakage. This phenomenon is consistent with a number of other studies [12, 13], and can be explained by floc rearrange or re-structure [6, 7]. In addition, because the surface bonding around the periphery are destroyed as the result of higher shear rate, some inner pores hidden by these aggregates were re-available to other small but compact clusters or particles. If they are filled up by those clusters or particles, the fractal dimension of flocs would evidently increase.

4.2. Floc size and strength characterization

The aggregates size distribution is another important parameter, which directly reflects the evolution of colloid aggregates. Moreover, the size distribution has a tight relationship with fractal dimension and strength of aggregates [38].

As shown in Fig. 3, after the slow stirring phase, flocs formed in stable 40 rpm have reached a d (50) floc size of 600 μm and flocs developed under gradually increased shear rates have d (50) floc size of 450 μm under the charge neutralization (Fig. 3a). The flocs, grown under stable 60 rpm and 60 + 40 conditions, exhibit some decrease after reaching the peak of size. Similar phenomenon was observed by Gregory and Rossi [15]. Unfortunately, the reasons for this behavior are not fully understood [25]. In all cases, floc size is immediately decreased sharply during the following increased shear. After breakage, flocs are exposed in the 40 rpm shear rate about 20 min, the d (50) size of all flocs regrows to another new plateau. Flocs formed in “40 + 60” and “60 + 40” conditions have larger size than other flocs, while flocs developed under stable 60 rpm are the smallest.

Flocs formed in “40 + 60” conditions and in stable 60 rpm, d (90) distribution shows different behavior compared with other flocs under charge neutralization (Fig. 3b). Especially the size of “40 + 60” flocs only slightly decreases during the breakage stage, while the pattern of breakage and regrowth behavior of the other three flocs.
is similar to $d$ (50) at the charge neutralization point. The reason may be that the strength of flocs formed in “40 + 60” condition is larger than other flocs. 

Table 2 shows the strength factors and recovery factors.

The strength factor values in Table 2 show that “40 + 60” flocs and “60” flocs have better ability to resist shear with larger strength factors. Thus, the associated size change at the breakage stage is smaller than the other two conditions. After breakage, floc regrowth is observed with recovery factor of 63% and 67% for “40 + 60” and “60” flocs respectively, while flocs formed in stable 40 rpm has the lowest recovery factor of 37%. Obviously, the flocs grown in gradually increased shear have better capability to resist the hydraulic shear than the “40” flocs.

Taking account of the method introduced in Section 2, strength of fractal aggregates can be calculated as shown in Table 3.

It can be seen that the sequence of floc strength is “40 + 60” > “60” > “60 + 40” > “40” during charge neutralization. The result is consistent with the results in Table 2. It indicates that not only the bonding forces between primary particles, but also the distribution of porosity plays a significant role in the strength of aggregates. Because the smaller clusters or particles fill the inner porosity of aggregates when the shear rate increases, the porosity of aggregates will decrease and the strength of aggregates will be improved. Thus, as shown in Fig. 3, some large size aggregates could survive during the high shear rate.

Table 3(b) shows the floc strength at the end of regrowth stage. The flocs formed in “40 + 60” conditions are stronger than other flocs. This phenomenon also reflects that “40 + 60” flocs have better performance to resist the fluctuation of hydraulic conditions. The decrease percentage of “40” flocs is negative reveals that the strength of “40” flocs is enhanced after breakage because the structure is more compact than which before breakage.

Table 3

| Runs  | $d_f$ (µm) | $d_0$ (µm) | $DF$ | $t_B$ | Decr. Perc. (%) |
|-------|------------|-------------|------|-------|----------------|
| 40 + 60 | 397.8      | 4           | 2.54 | 0.0091F | 28.6          |
| 60     | 380.1      | 4           | 2.52 | 0.0099F | 31.7          |
| 60 + 40| 446.9      | 4           | 2.48 | 0.0065F | 33.7          |
| 40     | 595.7      | 4           | 2.45 | 0.0049F | 30.3          |

$D_f$; mean of the last three $D$ [3,4] measured before breakage. Decrease Percentage: calculated by $(1 - t_B)$ ($t_B$ in Table 3(a)) × 100%

4.3. Size distributions of charge-neutralization flocs

Fig. 4 showed the bimodal distributions of colloid aggregates size during the breakage stage at the charge neutralization point. The peak of size distribution in 40 + 60 is around 100 µm and 500 µm, while the peak of stable 40 rpm shear condition is around 100 µm and 450 µm. Obviously, the smaller peaks under both shear conditions are almost same except different percentage. But the larger peaks have visible differences. Especially, the percentage of colloid aggregates larger than 400 µm in 40 + 60 is much greater than that of in stable 40 rpm shear condition and increases with the time during the breakage stage.

The percentage of flocs around the 450 µm formed in the 60 + 40 is larger than flocs formed in “40 + 60”. It seems contradictory with the results of Tables 2 and 3. It is obviously that the peaks of “60 + 40” flocs decreased as the development of breakage stage, while other flocs almost have the same size and volume during the breakage stage. According to Eq. (8), the strength at this shear rate is lower than the others. This is the reason why there is obvious decreasing of peak during the breakage stage. However, because the primary clusters which formed the “60 + 40” flocs grew at the relatively higher shear rate than “40” flocs, these clusters are more compact and stronger than “40” flocs but weaker than “60” flocs. Another seemingly inconsistent phenomenon is that the flocs formed in 60 rpm conditions have higher percentage of flocs around 500 µm. However, if pay attention to the flocs larger than 800 µm, it is obviously that the volume percentage of “40 + 60” flocs is about 6%, while other flocs is less than 1%. In addition, 40 + 60 flocs and 60 flocs have about 35% and 30% between 300 µm to 800 µm. This coincides with the results in Table 3.

5. Potential application in the engineering aspects

The strength of flocs influences the efficiency of water treatment reactors. Therefore, compact and strong flocs play a key role in the design of the effective flocculation or coagulation reactors. Moreover, they are influenced by the cavities distribution in flocs. Enhanced flocculation process by means of decreasing the large pores may be an aspect to improve the solid/liquid separation efficiency in coagulation and flocculation. And the reactors that can produce the gradually increased shear rate will be an economic and practical method to achieve this aim.

Floc structure is key factor to analyze the characters of flocs. To obtain the desired structures, we can control and optimize the influencing factors involved. The prediction of flocs dynamic behavior can be derived theoretically by the above theoretical model. Thus, we can not only improve the design of flocculation reactors, but
also promote optimization the existing reactors for desired engineered floc structure. The gradually increased shear rate may be an economic and practical method to improve the strength of flocs.

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