I. INTRODUCTION

Wireless power transfer (WPT) based on inductively coupled resonance was first introduced in [1], where an efficiency of about 40% was achieved with a separation of approximately 2 m between Tx and Rx of spiral shapes. Since then, the inductively coupled resonant WPT technology has been developed in theory and also applied to many applications including WPTs to multiple receivers, electric mobile phones, home appliances, motor vehicles, biomedical devices, and so on [2–6]. In most practical WPT devices, the information of power-receiving units needs to be transferred to power-transmitting units. There may be a variety of information but the identification numbers, stored power levels, etc., are essentially required in the basic operation of WPT devices. To cope with this necessity, the simultaneous wireless and information power transfer (SWIPT) has been studied in various forms of geometry and for the possible merging of information and power in the near future [7–10]. However, most of the research papers in this area focus on the numerous architectures in the high level of the hierarchy. However, some papers focusing on actual structures enabling information transfer in the current WPT frame are at times available, under the name of wireless power and information transfer (WPIT).

In [11], theory of high-order modulation for near-field RF identification (RFID) and WPT was presented. A system that transmits power using a triangular current waveform and transmits information to its third-order harmonic was reported in

Design of Wireless Power and Information Transfer Systems Considering Figure of Merit for Information
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Abstract

Inductively coupled resonant wireless power transfer (WPT) systems can be used as a wireless power and information transfer (WPIT) system by properly adding the function of varying Rx loads. A new metric for the figure of merit for information transfer from Rx to Tx is proposed as the ratio of Tx input impedances for the Rx shorted and optimum loads to systematically assess the information transfer. While most of WPT and near-field communication (NFC) devices have been adopted for very short distances between Tx and Rx, this work shows that the WPIT systems using inductively coupled resonant structures with high Q-factor coils enable much longer working distances with the best power transfer efficiency and information transfer capability. Several design examples show that the newly proposed figure of merit for information transfer is an essential metric in the understanding and design of WPIT systems. The theory is validated with circuit and electromagnetic simulations for various system configurations.

Key Words: Figure of Merit for WPT, Magnetic Coupling, Near-Field Communication, Simultaneous Wireless Power and Information Transfer.
In [12], a WPIT technology based on binary frequency shift keying modulation using the dual bands of a series-parallel combined resonant circuit was proposed. Its experimental prototype exhibited a communication rate up to 20 kbps, while maintaining a power transfer efficiency greater than 85% at a distance of 50 mm. However, these systems are complex in configuration. In [14], a frequency-agile load modulation scheme was proposed for a reliable near-field magnetic resonance WPT system. A wireless power and bidirectional data transmission scheme through mutual coupling between two isolated LC resonators was proposed in [15]. The near-field communication (NFC) [16] used for RFID technology may also be promising for delivery of this information by means of load modulation techniques. The existing NFC and other WPIT demonstrations are practically limited within a distance of several centimeters.

In this paper, we use simple mathematical expressions to analyze a WPIT system in terms of power and information transfer capabilities. Then, we provide design equations for a specifically required efficiency and transfer capability of Rx status information. Especially, to assess the information (including Rx status) transfer capability from Rx to Tx in a systematic manner, we propose a new metric using the input impedances at the Tx terminal depending on Rx loads. Its effectiveness and usefulness is validated by several design examples.

In Section II, the WPT performance of a single-input multiple-output (SIMO) system in terms of input impedances, efficiencies, and optimum loads for maximum efficiency are briefly discussed. Then, we newly define the figure of merit for information delivery using Tx input impedance variations depending on Rx load variations and demonstrate its usefulness. In Section III, we present some practical examples to validate the proposed WPIT methodology with electromagnetic (EM)-simulated results. The conclusions and closing comments are in Section IV.

II. DESIGN THEORY

Fig. 1 shows the equivalent circuit of a WPIT system. The system is composed of Tx0 (or Tx) and Rx1 (or Rx) coils (or loops), which may be a single-turn loop or a multi-turn loop or a spiral coil, separated by a certain distance \( d \). The loops, having inductances, are loaded with capacitors for LC resonance. The power is transferred from Tx to Rx via magnetically coupled resonant loops. \( R_i \) and \( L_i \) are the resistance and inductance of the Tx (\( i = 0 \)) and Rx (\( i = 1 \)) loops, respectively. \( C_i \) is the capacitance of the lumped capacitor for Tx (\( i = 0 \)) and Rx (\( i = 1 \)), respectively. \( r_i \) is the radius of the \( i \)th loop and \( r_{\text{in},i} \) is the inner radius of the \( i \)th loop wire. \( V_0 \) is the voltage at the input. The single-pole single-through (SPST) switch is operated between off (for an optimum load) and on (for a shorted load). The usual function of the Rx matching circuit is to transform the usually small Rx optimum load to the large device load (say, 50 \( \Omega \)). Conventional WPT has been made with the switch off to achieve maximum efficiency. The Rx status information (such as a device identity, energy charged levels, etc.) can be transferred from Rx to Tx by switching between the on and off states of the SPST.

Based on this equivalent circuit, the system is usually formulated by a \( Z \)-matrix given by

\[
\begin{bmatrix}
V_0 \\
0
\end{bmatrix} =
\begin{bmatrix}
Z_{00} & Z_{01} \\
Z_{10} & Z_{11}
\end{bmatrix}
\begin{bmatrix}
I_0 \\
I_1
\end{bmatrix}
\]

where \( k \) is the coupling coefficient between Tx and Rx loops [17]. It is well known that \( k \) approaches 1 as the distance between Tx and Rx becomes 0 and it approaches 0 as the distance between Tx and Rx becomes very large. \( V_0 \) is the source voltage, \( R_L \) is the Rx load resistance, and \( \omega \) is the angular frequency. \( I_0 \) and \( I_1 \) are the currents on loop 1 and 2, respectively. The ratio of currents on Tx and Rx loops is given by [18]:

\[
\frac{I_1}{I_0} = \frac{j\omega \sqrt{L_0L_1}}{R_i + R_L + j\omega L_i + \frac{1}{j\omega C_i}}.
\]

It is observed that as \( R_i \) increases, (2) becomes small and approaches 0 as \( R_i \) goes to infinity (open). The phase of the current flowing on Rx (\( I_1 \)) is 90° ahead of that flowing on Tx (\( I_0 \)) following Faraday’s law. The input impedance is defined as the ratio of \( V_0 \) and \( I_0 \) on a Tx terminal and expressed as

\[
Z_{in}(\omega, R_L) = \frac{V_0}{I_0} = Z_{in} + \frac{I_1}{I_0},
\]

\[
= R_i + j\omega L_i + \frac{1}{j\omega C_i} + \frac{(\omega k)^2 L_0 L_1}{R_i + R_L + j\omega L_i + \frac{1}{j\omega C_i}}.
\]
At the resonant frequency, the input impedance (3) reduces to

$$Z_{in}(\omega_0, R_L) = R_0 + \frac{(\omega_0 k)^2 L_0 L_1}{R_1 (1 + R_L / R_1)},$$

(4)

If we define the figure of merit for the power transfer ($F$) as

$$F = k Q_0 Q_1 = k Q \left( \frac{\omega_0 L_0}{R_0}, \frac{\omega_0 L_1}{R_0} \right),$$

(5)

the input impedance (4) at the resonant frequency depending on the Rx load $R_L$ can be re-written as

$$Z_{in} = R_0 \left( 1 + \frac{F^2}{1 + R_L / R_1} \right),$$

(6)

which is a purely real number. At this point, the essential part of power transfer efficiency for a resonant WPT system needs to be summarized [17]. The efficiency can be stated in a simple manner by

$$\eta(F, b) = \frac{F^2}{\left(1 + b\sqrt{1 + F^2}\right) \left(1 + \frac{1}{b}\sqrt{1 + F^2}\right)},$$

(7)

where $b$ is the deviation factor against the Rx optimum load $R_{L,opt}$ defined by

$$b = \frac{R_L}{R_{L,opt}} = \frac{R_L}{R_L \sqrt{1 + F^2}}.$$

(8)

A short observation of (7) tells that it is a function of the figure of merit for power transfer ($F$) and $b$, and a large $F$ is merely a necessary condition for a high efficiency. The maximum efficiency is guaranteed with the additional condition of $b = 1$ ($R_L = R_{L,opt} = R_L \sqrt{1 + F^2}$).

Now, we examine the ways of transferring Rx status information (or others) to Tx. Monitoring (6) at the Tx terminal depending on $R_L$ is just like monitoring the current on Tx ($I_L$) depending on $R_L$ since $I_0 = V_0 / Z_{in}$. When $R_L = 0$ (short), the system is at the over-coupled limit, no power is transferred to Rx, and the efficiency (7) is 0. However, the largest current is induced on Rx and the magnetic flux back to Tx affects the Tx input impedance most significantly, and the input impedance becomes the largest: $R_0 (1 + F^3)$. With this, the Tx current $I_0$ becomes the smallest. When $R_L = \infty$ (open), no current is induced on the Rx loop, the system is at the under-coupled limit, no power is transferred to Rx, the efficiency (7) is also 0, the Tx is as if being isolated from Rx, and the Tx input impedance becomes that of its own: $R_0$. When $R_L = R_{L,opt} = R_L \sqrt{1 + F^2}$ ($b = 1$) (optimum for maximum efficiency), (6) becomes

$$Z_{in} = R_0 \left( 1 + \frac{F^2}{1 + \sqrt{1 + F^2}} \right) = R_0 \sqrt{1 + F^2}.$$

(9)

Table 1. Input impedances and transfer efficiencies depending on Rx loads at resonant frequency

| Load status     | $R_L (\Omega)$ | $b$ | $Z_{in}(\omega_0) (\Omega)$ | $\eta(\omega_0)$ |
|-----------------|----------------|-----|-----------------------------|-----------------|
| Short (over-coupled limit) | 0 | 0 | $R_0 (1 + F^2)$ | 0 |
| Optimum (critically-coupled) | $R_L \sqrt{1 + F^2}$ | 1 | $R_L \sqrt{1 + F^2}$ | $F^2 / (1 + \sqrt{1 + F^2})$ |
| Open (under-coupled limit) | $\infty$ | $\infty$ | $R_0$ | 0 |

The current variations on Tx (or the input impedance variations) depending on $R_L$ (open, short, optimum) can be used for the information transfer from Rx to Tx. These input impedances (6) and the power transfer efficiencies (7) are summarized in Table 1.

NFC [16] more or less utilizes these variations of $Z_{in}$ at the Tx terminal occurring between the two load states of Rx, but mostly at a close proximity of Tx to Rx. Using the results in Table 1, we can assess the transfer capability of Rx information for the usual resonant WPT systems.

The best choice of the Rx load set for information transfer from Rx to Tx may be the short (over-coupled limit) and open (under-coupled limit) states, since this results in the largest current variation at the Tx with the effect of a lowest bit error rate. However, it is noted that with this choice, power is not transferred to Rx. The best Rx load choice for WPIT may be the short (for the greatest magnetic flux effect to Tx) and optimum (for the highest power transfer efficiency) loads. The real resistance of the SPST switch (Fig. 1) for the short state is not exactly 0. The practical resistance is about 10 mΩ but does not much affect the results in Table 1.

For the purpose of quantitative assessment by a new metric, we define the figure of merit for Rx information transfer to Tx ($F_I$) as a ratio of the Tx $Z_{in}$ when $R_L = 0$ and the same when $R_L = R_{L,opt}$ in Table 1, given by

$$F_I = \frac{Z_{in}(R_L = 0)}{Z_{in}(R_L = R_{L,opt})} = \frac{1}{\sqrt{1 + F^2}}.$$

(10)

The figure of merit for Rx information transfer to Tx ($F_I$) as defined in (10) also corresponds to the current ($I_L$) variation at the Tx terminal depending on Rx loads of “short” and “optimum” $R_L$ since $I_0 = V_0 / Z_{in}$. The metric (10) is plotted in Fig. 2 together with the maximum efficiencies as a function of the figure of merit for power transfer ($F$). We can see that as the figure of merit for power ($F$) increases, the figure of merit for information transfer ($F_I$) also increases and the power transfer efficiency also increases. Notice that when $F$ is roughly larger than 3, the efficiency is greater than 50% and $F_I$ almost ap-
Fig. 2. Figure of merit for Rx information transfer to Tx ($F_i$) and maximum efficiency ($\eta_{\text{max}}$) at the resonant frequency as a function of figure of merit for power ($F$) for a WPIT system.

approaches $F$. Taking an example, the transfer efficiency of about 80% is achieved with $F = 9$, where $F_i$ is also about 9.

### III. Design Examples Validated with Electromagnetic Simulations

The real resonant WPT systems realized for an $F$ given by (5) are numerous. Several realizations for a system consisting of a Tx loop with $r_0 = 10$ cm and a Rx loop with $r_1 = 5$ cm are shown in Table 2, where the quality factor $Q$ is the geometrical mean of $Q_0$ and $Q_1$ (5). The coupling coefficients $k$ were obtained using [16].

In Table 3, we summarize the same as in Table 2 but for a different system with larger Tx and Rx loops with $r_0 = r_1 = 20$ cm, enabling power and information transfer in longer ranges. It is seen in Table 3 that an efficiency of 56% is achieved for the case of $d = 80$ cm with $F_i = F = 7.3$. The figure of merit for power ($F$), one important parameter in the resonant WPT efficiency, can now be understood as the Tx current variations used for Rx information transfer.

We take the two system configurations with $d = 15$ cm and 25 cm in Table 2 and plot the real part (a) and imaginary part (b) of the input impedance (3) for different loads of $R_L = 0$ and $R_L = R_{\text{opt}} = R_L \sqrt{1 + F^2}$ as a function of frequency in Fig. 3. The radii of Tx and Rx loops are 10 cm ($Q_0 = 388.8$) and 5 cm ($Q_1 = 334.2$), respectively. The Tx and Rx loop wire radii are 0.1 cm. The imaginary parts (b) of the input impedances for both cases of $d = 15$ cm and $d = 25$ cm are observed to be zero at the resonant frequency since the system is at resonance. The real parts (a) of the input impedances at the resonant frequency, given by (6) and in Table 1, have the maximums when $R_L = 0$.

The circuit-simulated figures of merit for information transfer ($F_i$) are $3.7/0.5 (= 7.38)$ for the case of $d = 15$ cm and $0.42/0.17 (= 2.48)$ for the case of $d = 25$ cm. The EM-simulated figures

![Fig. 3. Input impedances of SISO system for different loads ($r_0 = 10$ cm, $r_1 = 5$ cm, $r_{\text{oxm}} = r_{\text{oxf}} = 0.1$ cm, $Q_0 = 388.81$, and $Q_1 = 334.23$): (a) real parts and (b) imaginary parts.](image)
of merit for information transfer \((F_i)\) are 3.26/0.45 (\(= 7.2\)) for the case of \(d = 15\) cm and 0.33/0.16 (\(= 2.1\)) for the case of \(d = 25\) cm. The results are in agreement with the theoretical ones of 7.4 and 2.5 in Table 2. These \(F_i\)s should be understood as the Tx current variations due to the Rx load changes. The overall EM-simulated input impedances are shown to be in good agreement with the theoretical ones.

Fig. 4 shows the transient responses of the Tx currents when the Rx load switches between with \(R_L = 0\) and \(R_L = R_{L, \text{opt}} = R_{\text{t}} \sqrt{1 + F^2}\) with 10 kbps (a) and 20 kbps (b) for the case of \(d = 15\) cm and \(Q = \sqrt{Q_1/Q_2} = 360.5\) in Table 2. Based on the AC steady state analysis, the Tx current variation (characterized by \(F_i\)) with each Rx load has been found to be almost identical to the theoretical value of 7.4. Based on the transient analysis with increasing switching rates, Fig. 4(a) and 4(b) show that it takes about 0.5 ms for the Tx current to reach a steady state. The source voltage \(V_0\) in Fig. 1 is assumed to be 1 V. For the shorted Rx load with \(R_L = 0\) Ω and optimum load with \(R_L = 0.25\) Ω, the average Tx current envelopes are 0.33 A and 1.97 A, respectively, for the case of the 10 kbps switching rate (Fig. 4(a)). Thus, the ratio of the Tx currents is 6.0 (\(= 1.97/0.33\)). For the case of 20 kbps (Fig. 4(b)), the ratio of the Tx current envelopes is 5.0 (\(= 1.96/0.39\)). Even though the ratio of Tx currents somewhat deviates from the expected \(F_i\) due to the effects of the transients from switching operations.

Fig. 5 shows the same as plotted in Fig. 4 for the different configuration of \(d = 80\) cm and \(Q = \sqrt{Q_1/Q_2} = 776.2\) (\(F = 3.4, F_i = 3.6\)) in Table 3. The Tx current variation with the mentioned two Rx loads when reached in steady state is about 3.5 (close to the theoretical \(F_i = 3.6\)). The source voltage \(V_0\) in Fig. 1 is assumed to be 1 V. The short and optimum loads \((R_{L, s})\) are 0 Ω and 0.24 Ω. The ratio of Tx current envelopes is 3.3 for the case of 10 kbps and 3.1 for the case of 20 kbps, again close to the theoretical value \((F_i) = 3.6\).

The figure of merit for information transfer \((F_i)\) as defined in (10), expressed as a function of the figure of merit for power transfer \((F)\), has been shown to be very useful in characterizing and estimating the resonant WPIT systems, especially in their capability of transferring Rx information to Tx.
IV. CONCLUSION

A new metric named “a figure of merit for information transfer” has been defined to assess WPIT systems in their capability to transfer information from Rx to Tx. Its usefulness has been verified for several WPIT system configurations with wide ranges of Tx to Rx distances. It has been found to be close to the figure of merit for power and shown to be the ratio of the Tx currents when the Rx load is shorted and optimum. Introduction of the new metric is expected to put a basic foundation in the evaluation of WPIT systems which started being developed recently.

This research was supported by the Ministry of Science, ICT and Future Planning, Korea, under the Information Technology Research Center support program (No. IITP-2020-2016-0-00291) supervised by the IITP (National IT Industry Promotion Agency).

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