HVC-Net: Unifying Homography, Visibility, and Confidence Learning for Planar Object Tracking

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Abstract. Robust and accurate planar tracking over a whole video sequence is vitally important for many vision applications. The key to planar object tracking is to find object correspondences, modeled by homography, between the reference image and the tracked image. Existing methods tend to obtain wrong correspondences with changing appearance variations, camera-object relative motions and occlusions. To alleviate this problem, we present a unified convolutional neural network (CNN) model that jointly considers homography, visibility, and confidence. First, we introduce correlation blocks that explicitly account for the local appearance changes and camera-object relative motions as the base of our model. Second, we jointly learn the homography and visibility that links camera-object relative motions with occlusions. Third, we propose a confidence module that actively monitors the estimation quality from the pixel correlation distributions obtained in correlation blocks. All these modules are plugged into a Lucas-Kanade (LK) tracking pipeline to obtain both accurate and robust planar object tracking. Our approach outperforms the state-of-the-art methods on public POT and TMT datasets. Its superior performance is also verified on a real-world application, synthesizing high-quality in-video advertisements.

Keywords: Planar Object Tracking, Homography, Visibility, Confidence

1 Introduction

Planar object tracking is a classic computer vision task with a wide range of applications. Given the initial corners of a planar object in the reference frame, the primary goal of planar tracking is to estimate the movements of these corners, modeled by a geometric transformation called a homography, in consecutive frames. Though lots of advances have been made in past decades, obtaining accurate and robust results remains challenging. These difficulties are mainly caused by three factors: appearance variation, camera-object relative motion and occlusion. The appearance variation is a camera-related issue. It is usually known as image blur, sensor noise, non-linear response of brightness. The camera-object
relative motion leads to geometry transformations of an object on the image. Typical effects on the image plane are scale changes, rotations, translations, and perspective distortions. Occlusion is referred as the fact that the tracked object is occluded by another object. The situation becomes worse if the ‘another object’ looks very similar to the tracked object. These factors pose strong challenges for traditional keypoint-based methods that estimate the homography using hand-crafted features [35, 12, 6], since the extracted features are prone to be different under the influence of these factors. Learned features like D2-Net [14], LF-Net [45], and R2D2 [30] are proposed to decrease this influence. Direct methods [4, 7], usually with the LK pipeline [4], estimate the homography iteratively. [4, 7] assume the intensity consistency and compute the homography increment for each iteration. [9, 27, 24, 46, 47] extend direct methods with the learned ‘feature consistency’ assumption for increasing the robustness. We argue that efforts are still needed on better feature representation. Moreover, these methods have not discussed occlusions that are widely existed in real-world video sequences. The last to mention is the CNN-based method [11] that directly regresses the homography in one step with CNN. It is not robust to these three factors, neither.

In this work, we propose a novel CNN model for handling mentioned difficulties. The base of our model is correlation blocks (Sect. 3.3). It firstly extracts features in the intensity domain for handling appearance variations. Cost volumes, representing distributions of pixel correlations, are then constructed in the pixel displacement domain to account for the camera-object relative motion. We find that estimating the homography with these two cascaded steps is much better than methods with one step [11, 27, 9, 24]. Moreover, in contrast to methods that learn homography alone [11, 27, 9, 24], we learn it jointly with another task called visibility, which is defined as a binary mask that indicates which part of the reference image is visible on the tracked image (Fig. 2). A reference image pixel is regarded as visible if and only if it satisfies the homography constraint of the tracked planar object (geometry-induced) and it is not occluded by other objects on the tracked image (disocclusion-induced). Joint learning homography and visibility not only improves the correlation block representations, but also links camera-object relative motions with occlusions (Sect. 3.5). Lastly, as estimations with the LK pipeline are sensitive to initializations, we further improve
the estimation robustness by monitoring the tracking quality and rebooting estimations. This is done by introducing a confidence module that evaluates the planar tracking quality from pixel correlation distributions obtained in correlation blocks (Sec. 3.7). By equipping all these presented modules with a LK pipeline, our model obtains both accurate and robust homography estimations. We achieve significantly higher homography precision than state-of-the-art homography estimation methods (Sect. 4). Besides, as a by-product, our model provides visibility masks that other works have not mentioned. With these masks, we are able to easily place planar advertisements in videos (Fig. 1).

2 Related Work

2.1 Homography Estimation

Existing planar tracking methods for estimating the underlying homography can be roughly classified into three categories: keypoint-based methods [35, 12, 6, 28, 3, 13], direct methods [4, 7, 10, 31, 5, 26], and CNN-based methods [11, 27, 9, 24]. Keypoint-based methods firstly detect and describe keypoints (using ORB [35], SIFT [12], SURF [6] and etc.) both in the reference planar region and subsequent consecutive frames. These keypoints are then matched by minimizing the distances in the descriptor space. Homography, the planar surface in the projection space is related, is then calculated with the obtained matches. To remove potential outlier matches, RANSAC [16] is usually performed. Different from keypoint-based methods, direct methods [4, 7] assume that the planar template does not move fast in consecutive images. The homography is directly optimized by minimizing the photometric error between the planar template and its projection in the incoming video frames. Recently, CNN-based methods have been proposed. Homography is regressed from input images in one forward step [11, 27, 46, 47]. [9, 24, 20, 48] adopt the Lucas-Kanade framework [4] and compute homography with multiple iterations.

2.2 Object Segmentation

The visibility of planar object tracking is less discussed in the past. The closest work is segmentation. There are three main approaches for object segmentation according to the level of supervision required. Supervised methods require iterative human interactions for adding segmentation prior as well as refining segmentation outputs [2, 15]. They obtain high-quality segmentations at the cost of
extensive expert efforts. To relax this mass manual supervision, semi-supervised methods propagate sparse human labeling in the reference frame to the remaining frames, and then formulate the segmentation problem as an optimization problem with energy defined over graphs [1, 29, 42]. The last to mention is the unsupervised methods that do not require any manual annotation or utilize prior information on the segmented objects. Early unsupervised methods focus on over-segmentation [17] or motion segmentation [8]. They are extended to foreground-background separation in recent years [44, 41].

2.3 Patch Similarity

The most related work to confidence prediction is to compute the similarity between two patches [36, 18, 37]. The confidence score is learned by training the network with reflective loss in [37]. The similarity is trained via a classification pipeline in [36]. Patched representation as well as robust feature comparison is jointly learned in [18].

3 Our Approach

3.1 The LK-based CNN Framework

Our model framework is shown in Fig. 3. We follows the LK scheme [4] to compute homography, denoted as $H_{ij} \in \mathbb{R}^{3 \times 3}$. For each 3D object point $o_k$, its
projection on image frame \(i\) and \(j\) is denoted as \(p^k_i\) and \(p^k_j\) respectively. According to the derivation from [19], we have \(p^k_i = H_{ij} p^k_j\). Supposing we have an initial homography \(H_{ij}\), the LK scheme consists of two iterated steps:
1) solving for homography increment \(\delta H_{ij}\),
2) updating homography \(H_{ij} \leftarrow H_{ij} \ast \delta H_{ij}\).

For the first step, the classic LK method [4] assume that intensities are consistent across images. We improve this step with three aspects. Firstly, as the intensity consistency assumption is prone to be broken in real-world cases with appearance variations and occlusions, we extend it with the ‘feature consistency’ assumption and improve the effectiveness of feature representation (Sect. 3.3). Secondly, homography increments are computed with difference scales (Sect. 3.4). Thirdly, based on the ‘feature consistency’ assumption, we compute homography increments with joint homography and visibility learning (Sect. 3.5). The improved first LK step is implemented as the multi-scale motion estimation module in our model. We also have an optional step without correlation block, i.e. the refinement module (Sect. 3.6). As computed homography increments are sensitive to homography initializations, we present a tracking confidence module to evaluate the estimation quality and re-initializes the homography computations (Sect. 3.7). We follow the same second step as the LK pipeline, where we update homography through update layers. Lastly, we notice that the concerned planar object tracking problem is to solve for homography between object projections on two images while existing LK-based methods consider homography between two images. We thus propose a sampling trick to turn the concerned problem into a classic LK-based homography problem that is more suitable for CNN models (Sect. 3.2).

### 3.2 Homography Surrogate & Sampling

The projection shape of a 3D plane on video images deforms as the camera moves relatively to the tracked object. Processing the full-resolution video images with CNNs will waste a lot of memory as well as computations on useless image regions outside the projection shape. What’s worse, information on outside regions will distort the estimations and make CNN predictions more challenging. To this end, we propose a planar object sampling layer for CNNs for handling planar objects in arbitrarily deformed shapes or sizes. As shown in Fig. 4, the key idea is NOT to predict the original homography in the original image space. Instead, we predict a surrogate homography in the normalized space. We sample the planar object in the reference image into a \(W \times H\) template: \(p^n_i = H^n_i p_i\), where \(H^n\) can be easily computed using SVD [19] once the reference planar object with four-corner representation is given. We denote the homography used to sample the planar object in the current image into a \(W \times H\) template as \(H^n_j\), and the homography between two normalized images \(i\) and \(j\) is \(H^n_{ij}\). We have:

\[
H^n_j = (H^n_{ij})^{-1} H^n_i H_{ij} = (H^n_{ij})^{-1} H^n_{ij}
\]

where \(H^n_{ij} = H^n_i H_{ij}\). We define \(H^n_j\) as a surrogate for \(H_{ij}\), and \(H^n_{ij}\) as a surrogate for \(\delta H_{ij}\). \(H^n_{ij}\) will be an identity matrix if and only if \(H^n_{ij}\) is equal to ground
Fig. 4. The planar object sampling. We sample the planar object in the reference frame and in the current frame to fixed-size images with $H^n_i$ and $H^n_j$, and use our mode to predict the increment $H^s_{ij}$. $H^s_{ij}$ will be the identity matrix if and only if the sampled planar objects on both sampled images are aligned perfectly. $H^n_j$ and $H^s_{ij}$ are used as surrogates for $H_{ij}$ and $\delta H_{ij}$ respectively.

truth $H^*_ij$. If the final $H^n_j$ is obtained, $H_{ij}$ is computed as $H_{ij} = (H^n_i)^{-1}H^n_j$. By using surrogates, we maintain a fixed-size input to CNNs.

3.3 Correlation Block

Different from previous works [11, 24] that regress homography on images, we decompose the homography regression into two cascaded steps:

1) The first step is to extract features representing image local appearances. These features are designed to be robust for image blur, illumination variations, occlusions, scale changes, perspective distortions, etc, through data argumentation covering various image conditions. Since the template size is small, we use the U-Net structure [32] for simplicity. Other feature extraction structures, such as ResNet, EfficientNet and MultiResUNet, can also be used.

2) The second step is to construct cost volumes with extracted features, whose elements are pixel correlations between sampled images. These pixel correlations are designed to encode the relative geometry transformation between objects and cameras. Each element in this cost volume is computed as the correlation [40] between a pixel $x_i$ in reference feature map $f_i$ and a pixel $x_j$ in the tracked feature map $f_t$: $c(x_i, x_j) = f_i(x_i)^T f_t(x_j)$, where $T$ is the transpose operator. Given a maximum displacement $d_m$, for each location $x_i$ we compute correlations $c(x_i, x_j)$ for $x_j$ s.t. $|x_j - x_i| \leq d_m$. Correlations at each location $x_i$ are reorganized in the channel dimension. Thus, the size of the 3D cost volume is $H \times W \times (2d_m + 1)^2$. $d_m$ is set to be 4 at each pyramid here by balancing the complexity and movement range.
3.4 Pyramids

Inspired by the classic pyramid methods in image processing, we build correlation blocks in different scales. We sample objects with different template resolutions (1/16x, 1/4x, 1x). Homography increments are computed sequentially from the smallest resolution to the highest resolution.

3.5 Joint Learning of Homography and Visibility

Homography is obtained by information that is visible on both reference and tracked images. Hence, we learn homography jointly with visibility, in order to extract a more reliable feature representation. This leads to three loss functions during training: $L_d$, $L_m$, and $L_v$. For benefit of CNNs, we adopt representation in [11], where homography is represented by four corner displacements $\{d_1, d_2, d_3, d_4\}$. $L_d$ is a homograph loss. It is defined as the $l_1$ norm between the ground truth 4-point displacement $d^*_k$ and the predicted 4-point displacement $d_k$ at each scale level:

$$L_d = \frac{1}{4} \sum_{k=1}^{4} \|d^*_k - d_k\|_1$$

$L_m$ is a visibility loss. Pixel visibility prediction of the sampled tracked image is regarded as a 2-class classification problem. We denote the ground truth label and the predicted label for a pixel’s visibility as $m^*_k$ and $m_k$. Cross-entropy is adopted for the visibility loss $L_m$ at each scale level:

$$L_m = -\frac{1}{N^k} \sum_{k=1}^{N^k} (m^*_k \log(m_k) + (1 - m^*_k) \log(1 - m_k))$$

where $N^k$ is the total number of pixels at each scale level. To further improve the feature representations used to construct cost volumes, we add a visible alignment loss $L_v$ that minimizes the visible feature distance between extracted reference feature map $f_r$ and tracked feature map $f_t$. It is defined as followed,

$$L_v = \frac{1}{N^k} \sum_{x_k} m_k \|f'_t(x_k) - f_t(x_k)\|_1$$

where $x_k$ is the pixel location on the sampled tracked image, $f'_t = \text{Warp}(f_r, H_{tr})$ is a wrapped feature map from $f_r$ to $f_t$ using the homography $H_{tr}$. The total loss is the combination of these three losses:

$$L_{all} = \lambda_d L_d + \lambda_m L_m + \lambda_v L_v$$

where $\lambda_d$, $\lambda_m$ and $\lambda_v$ are balancing parameters. In our experiments, they are all empirically set to be 1.0.

With the visibility loss, we explicitly connect homography with occlusion. This is in contrast to competing methods [9, 27, 24, 46, 47] that handle occlusions implicitly with the learned feature capability. Moreover, with the visible alignment loss, we able to connect homography, visibility and features in the correlation block.

Notice that, the supervised visibility mask varies in each scale level. It is generated at each training iteration.
3.6 Homography and Visibility Refinement

This module is similar to that of Sect. 3.5 expect that the correlation block is removed and the visible alignment loss is ignored. It is designed to capture tiny modifications to the homography and visibility. The VGG structure [39] is used for simplicity. Three iterations are usually conducted for convergence. Note that, this module is optional.

3.7 Estimation Confidence Evaluation

This section discusses the homography initialization in the LK pipeline (Sect. 3.1). The initial homography of the first scale level is equal to the homography obtained at the previous video frame \( j - 1 \). For the following scale levels, their initializations are equal to homography obtained at previous scale levels. For the refinement module, its first homography initial value is equal to the homography output from the multi-scale motion estimation module. In the following refinement step, its initial homography is equal to the homography in last iteration.

With this homography initialization mechanism, we see the significance of the homography obtained at the previous video frame \( j - 1 \), as it is the base of estimation in the current video frame \( j \). However, though we have tried our best to improve the homography estimation robustness and accuracy, our trained model inevitably fails under extreme conditions, such as large appearance variations, rapid camera-object relative motions, and severe occlusions. That is, the homography obtained at the previous video frame \( j - 1 \) may be unreliable. To check this, we add a tracking confidence module to evaluate the estimation confidence. This confidence is regarded as a regression whose output ranges between 0 and 1. 0 indicates the estimation is unreliable while 1 indicates it is reliable. In contrast to previous works [36, 18, 37] that regress confidences from images, we regress them from cost volumes of correlation blocks. These multi-scale cost volumes, representing distributions of pixel correlations, encode the ‘uncertainty’ of the estimation. For an object pixel in the reference image, its corresponding pixel on the tracked image is ambiguous if the pixel correlation distribution is flat, or obvious if the pixel correlation distribution is concentrated on one specific location. We train this tracking confidence module after the multi-scale motion estimation module and the optional refinement module is trained using an independent dataset.

We consider the estimation as unreliable if the homography loss \( L_d \) between the ground truth and predicted homography is larger than 5 while reliable otherwise. We denote the ground truth label and the predicted label as \( p^* \) and \( p \). Cross-entropy loss is used for confidence loss:

\[
L_c = - (p^* \log(p) + (1 - p^*) \log(1 - p))
\]  

(6)

In implementations, each cost volume of each pyramid layer is convoluted to a \( H_8 \times W_8 \times 15 \) feature map by several convolutional layers respectively. These feature maps are then followed by two fully connected (FC) layers, whose dropout ratio is set to 0.5, with 1024 and 2 channels. The final layer is a soft-max layer that output the confidence. 3 × 3 kernels are used in convolutional layers.
After the tracking confidence module is trained, we monitor the tracking
confidence on the fly. If the homography obtained at the previous video frame
\(j-1\) is classified as unreliable, we use the homography estimated in more previous
times (e.g. 2 to 60 frames before) for homography initialization and re-run our
model pipeline. This process is repeated until this tracking is reliable.

4 Experiments

Similar to [9, 11], we use the MS-COCO dataset [25] to generate the training
data. All images are resized to 240 × 240. We randomly select an image, assign
a 120 × 120 window to its center. We then randomly perturb the four corners of
this window to generate a random homography. The corner displacement is uni-
formly distributed between [-32, 32] in both horizontal and vertical directions.
Pixels within the perturbed window are wrapped to a sample image whose size
is \(W \times H\). To increase the robustness of our network, we augment our samples
with more conditions that we meet in real-world applications. We add variances
of brightness, contrast, saturation and image blur to the sample images [38].
Moreover, we simulate real-world object occlusions by randomly placing arbi-
trary polygons, whose textures are cropped natural images from [25], into our
training samples [38]. 280000 image pairs with ground truth homography are
generated in total (Fig. 5). Among them, 200000 samples are used for train-
ing the motion estimation network and refinement network, 40000 samples are
used for validation, and the rest 40000 samples are tested for ablation study
(Sect. 4.2). GT visibility masks are generated at each training iteration.

4.1 Training & Quantitative Evaluation

In all experiments, we set \(W = H = 120\). Adam [22] optimization with \(\beta_1 = 0.9, \beta_2 = 0.999\) is used, and the batch size is set to 32. Batch normalization [21] is
adopted for accelerating convergence. The learning rate is initialized to be $10^{-4}$. It is then decreased by a factor of 10 every 5 epochs. After the model is trained, its processing rate is about 10hz on a commodity GPU card GeForce GTX 1080.

In this paper, two quantitative metrics, alignment error (AE) [34] and homography discrepancy (HD) [23], are used to evaluate the quality of predicted homography accuracy.

### 4.2 Ablation Study

In this section, we perform ablation studies to analyze the contribution of each component in our proposed model. All methods are trained on the training dataset as well as tested on the dataset from Sect. 4 introduction.

**Homography Precision** We firstly analyze component contributions to the homography precision. We train our model with increasing components proposed in this paper: the correlation block in Sect. 3.3 (D), pyramids in Sect. 3.4 (P), joint learning of homography and visibility in Sect. 3.5 (M), the refinement module in Sect. 3.6 (R): Ours-D, Ours-DP, Ours-DPR, Ours-DPM, Ours-DPMR.

If our model is trained without any proposed components (Ours w/o DPMR), it is equivalent to DeepHomography [11]. Tab. 1 shows the results:

| Method         | AE [34] | HD [23] |
|----------------|---------|---------|
| Ours w/o DPMR  | 6.678   | 14.983  |
| Ours-P         | 5.280   | 10.627  |
| Ours-PR        | 2.970   | 5.104   |
| Ours-PM        | 4.051   | 7.984   |
| Ours-PMR       | 2.426   | 4.262   |
| Ours-D         | 4.173   | 9.147   |
| Ours-DP        | 1.145   | 2.216   |
| Ours-DPR       | **0.876** | 1.739  |
| Ours-DPM       | 1.097   | 2.107   |
| Ours-DPMR      | **0.876** | **1.695** |

- From line 2 and line 7, we see that the model with correlation blocks (Ours-D) performs significantly better than that without them (Ours w/o DPMR).
- Pyramids (P) do help both approaches (Ours-D and Ours w/o DPMR). This improvement is more significant for the model Ours-D as the cost volume is constructed on limited displacements.
- The refinement module is able to capture tiny displacement between images. It further increases the accuracy for all models (Ours-DP vs Ours-DPR, Ours-DPM vs Ours-DPMR, Ours-P vs Ours-PR, Ours-PM vs Ours-PMR).
- By jointly training homography and visibility, our model generalizes better on each original task (Ours-DP vs Ours-DPM, Ours-P vs Ours-PM, and Ours-PR vs Ours-PMR).
Visibility Accuracy  Apart from the improvement to homography precision, we wonder whether learning of homography and visibility jointly (M) leads to higher visibility accuracy than learning these two tasks independently (V). We also test if the correlation block helps visibility accuracy. We train four models on the generated training dataset: Ours-PMR, Ours-DPMR, Ours-PVR and Ours-DPVR. We then compute the visibility loss (Sect. 3.5) on the test set. Results are shown in Tab. 2. We find that the correlation block and joint learning not only help the homography predictions but also improve the visibility estimations. We see strong connections between homography and visibility. Visibility, a by-product of our work, can be used for in-video advertising. We show one synthesized frame (Fig. 6) using our obtained visibility during experiments on the POT dataset [23]. We meet large and irregular occlusions that are challenging to our model. Fortunately, our model is able to overcome this difficulty.

Confidence Effectiveness One way to evaluate the confidence effectiveness is to compute the classification statistics using the predicted confidence (0.5 is used as the threshold). We follow data generations in Sect. 4 introduction to generate an additional large dataset covering challenging conditions. This dataset, on which tracking is much harder than that of in Sect. 4 introduction, contains 50000 samples. The percents of training, validation and testing are 80%, 10% and 10% respectively. Our trained models (Ours-DPR and Ours-DPMR) are then run on this dataset. If the computed \( L_d \) is smaller than 5, the tracking result is labeled to be reliable. Otherwise, it is labeled to be unreliable. Obtained labels are adopted for training the confidence network and testing the confidence performance. PatchCon [36] that directly regresses this confidence from wrapped images is the baseline/competing method. Both OursCon and PatchCon are trained to evaluate pre-trained Ours-DPMR and Ours-DPR.

True-positive rate (TPR), false-positive rate (FPR), false-negative rate (FNR) and true-negative rate (TNR) are shown in Tab. 3. Comparing OursCon and PatchCon [36] that both evaluate Ours-DPMR, we see that tracking confidence
Table 3. Classification statistics using the estimated confidence.

| Method + Pre-trained Base | TPR  | FPR  | FNR  | TNR  |
|---------------------------|------|------|------|------|
| PatchCon [36] + Ours-DPMR | 93.1%| 14.5%| 6.9% | 85.5%|
| OursCon + Ours-DPMR       | 96.6%| 8.7% | 3.4% | 91.3%|
| OursCon + Ours-DPR        | 96.5%| 10.2%| 3.5% | 89.8%|

Fig. 7. Results obtained by our model in different conditions. (a) A planar object in the reference frame. (b) The tracked planar object in the current frame. (c) Predicted visibility mask corresponding to (b). (d) The synthetic frame after placing the CVF logo on (b). More results can be found in the supplementary material.

predicted from correlation blocks is more accurate. Moreover, from OursCon + Ours-DPR and OursCon + Ours-DPMR, we see that joint learning of visibility mask and homography does improve the effectiveness of our correlation block and model generalization, leading to performance gains of confidence prediction.

4.3 Comparisons on Other Datasets

Two public datasets, POT [23] and TMT [34], are used to evaluate the homography accuracy. State-of-the-art methods, including SIFT [12], SURF [6], L1 [5, 26], IVT [33], ESM [7], Gracker [43], DeepHomography [11], IC-STN [24], Ctx-Unsupervise [47], PFN [46], MHN [20] and DLKFM [48] are compared. Our models are all with our tracking confidence module (OursCon), except the one named Ours-DPMR w/o OursCon. The competing confidence prediction method, PatchCon [36], is also included for comparison (Ours-DPMR-PatchCon). The model with all our modules achieves the best performance.

POT is a planar object tracking benchmark containing 210 videos of 30 planar objects in natural environments. It contains scenes with various challenging conditions, including scale change, rotation, perspective distortion, motion blur, occlusion, out-of-view, and a combination of these factors. For better presentation, comparisons are shown with precision plots and success plots. Precision plot counts the percentage of frames whose AE is within the threshold $t_p$. Success plot counts the percentage of frames whose HD is within a threshold $t_s$. Results are
Table 4. Success rate of different approaches on the TMT dataset with AE < 5 \cite{34}. Larger is better. Best and second best are colored. (*) Models of Ours-DPMR, Ours-DPMR-PatchCon and Ours-DPMR w/o OursCon perform the same. We omit rested notations for short.

| Method             | Cereal | Book1 | Book2 | Book3 | Juice | Mug1 | Mug2 | Mug3 | Bus | Highlight | Letter | Newspaper |
|--------------------|--------|-------|-------|-------|-------|------|------|------|-----|-----------|--------|-----------|
| SIFT \cite{12}     | 0.92   | 0.73  | 1.00  | 0.84  | 0.89  | 0.91 | 0.43 | 0.55 | 0.19| 0.97      | 0.18   | 0.16      |
| SURF \cite{6}      | 0.91   | 0.64  | 1.00  | 0.74  | 0.50  | 0.07 | 0.14 | 0.06 | 0.19| 0.94      | 0.08   | 0.01      |
| L1 \cite{26}       | 0.24   | 0.10  | 0.79  | 0.42  | 0.16  | 0.10 | 0.30 | 0.54 | 0.57| 0.67      | 0.19   | 0.63      |
| IVT \cite{33}      | 0.99   | 0.48  | 0.30  | 0.72  | 0.98  | 0.91 | 0.72 | 0.68 | 0.94| 0.95      | 0.25   | 0.92      |
| ESM \cite{7}       | 1.00   | 1.00  | 1.00  | 0.34  | 1.00  | 0.89 | 1.00 | 1.00 | 0.76| 1.00      | 1.00   | 1.00      |
| Gracker \cite{43}  | 0.91   | 1.00  | 1.00  | 0.88  | 1.00  | 1.00 | 0.83 | 0.75 | 0.97| 1.00      | 0.78   | 1.00      |
| DeepHomography     | 0.92   | 1.00  | 1.00  | 0.82  | 0.99  | 0.93 | 0.65 | 0.80 | 0.50| 0.99      | 1.00   | 0.95      |
| IC-STN \cite{24}   | 0.92   | 1.00  | 1.00  | 0.82  | 1.00  | 0.77 | 0.79 | 0.99 | 0.98| 1.00      | 0.95   | 0.95      |
| PFN \cite{46}      | 0.74   | 0.28  | 0.92  | 0.38  | 0.39  | 0.89 | 0.40 | 0.88 | 0.24| 0.78      | 0.29   | 0.53      |
| Ctx-Unsupervise    | 0.54   | 0.38  | 1.00  | 0.38  | 0.29  | 0.28 | 0.23 | 0.39 | 0.16| 1.00      | 0.17   | 0.14      |
| MHN \cite{20}      | 0.62   | 0.18  | 0.92  | 0.40  | 0.63  | 0.95 | 0.50 | 0.41 | 0.50| 0.76      | 0.22   | 0.14      |
| DLKFM \cite{48}    | 0.58   | 0.18  | 0.92  | 0.41  | 0.63  | 0.99 | 0.50 | 0.41 | 0.50| 0.76      | 0.21   | 0.14      |
| Ours-D             | 0.85   | 0.65  | 0.84  | 0.67  | 0.37  | 1.00 | 0.78 | 0.72 | 0.71| 0.92      | 0.50   | 0.32      |
| Ours-DP            | 0.93   | 1.00  | 1.00  | 0.86  | 1.00  | 1.00 | 0.84 | 0.81 | 0.97| 1.00      | 1.00   | 0.93      |
| Ours-DPR           | 0.93   | 1.00  | 1.00  | 0.88  | 1.00  | 1.00 | 0.83 | 0.80 | 0.95| 1.00      | 1.00   | 0.98      |
| Ours-DPM           | 0.93   | 1.00  | 1.00  | 0.88  | 1.00  | 1.00 | 0.72 | 0.83 | 0.99| 1.00      | 1.00   | 0.93      |
| Ours-DPMR (*)      | 0.93   | 1.00  | 1.00  | 0.88  | 1.00  | 1.00 | 0.89 | 0.85 | 0.99| 1.00      | 1.00   | 1.00      |

shown in Fig. 8 and the supplementary material. Our proposed method shows superior performance in all scenes. Especially for scenes with motion blur, perspective distortion, scale change or combinations of these factors, our approach works much better because it is hard for non-learning algorithms to model the underlying variation or tuning related parameters manually.

TMT consists of sequences for manipulation tasks. There are 100 annotated and tagged sequences in total. Similar to POT, sequences in this dataset also have a large condition variation. We use the same evaluation metric as in \cite{34}. That is, the success rate that counts the percentage of frames whose AE < 5. Comparison results are summarized in Table 4. Overall, our model achieves a better or similar performance in all sequences compared to other methods.

We visualize some qualitative results obtained by our model during experiments and place a product (i.e. the CVF logo) on the tracked planar object in Fig. 1 and Fig. 7. More results can be found in the supplementary material.

5 Discussions & Limitations & Conclusions

The main limitation of our work is that the predicted visibility mask is not perfect. With the own constraints of LK-based methods, our approach is sometimes disturbed by the factor of similar occluded objects. In conclusion, we proposed a novel model for planar object tracking. Homography, visibility and confidence are jointly learned based on a correlation block. We achieved a superior planar tracking performance compared to state-of-the-art methods on the public dataset, provided visibility masks that other works had not discussed, calculated more reliable confidence than competing approaches. To better take multi-frame constraints and similar occlusions into consideration is our future work.
Fig. 8. The comparison of different approaches shown in precision plots on the POT dataset [23]. Curves with larger areas are better. The AE at threshold = 5 [34] is illustrated within brackets. Zoom-in is recommended. Video comparisons are in the supplementary material.
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