Signal Reconstruction of the ATLAS Hadronic Tile Calorimeter: implementation and performance

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Abstract. TileCal, the central hadronic section of the ATLAS Calorimeter, is a sampling calorimeter made of steel and scintillating tiles. The TileCal front-end electronics reads out about 10,000 photo-multipliers at 40 Msps measuring energies ranging from $\simeq 30$ MeV to $\simeq 2$ TeV. The read-out system is designed to provide the ATLAS High Level Trigger with reconstructed PMT signals within the time budget allowed by the First Level Trigger (LVL1) running at a maximum trigger rate of 75 KHz. The signal amplitude, time and a reconstruction quality factor are obtained for each PMT using optimal filtering techniques implemented in the Digital Signal Processors (DSP).

1. Introduction

ATLAS [1] is a general purpose experiment designed to explore the physics landscape in proton-proton collisions at the unprecedentedly high energy regime of the Large Hadron Collider at CERN. After many years of careful preparation ATLAS received the first collisions from LHC in December 2009. After a short overview of the Tile Calorimeter read-out system we will discuss the implementation of Optimal Filtering algorithms highlighting the constraints imposed by the use of DSPs. We will report on the validation of the DSP algorithm and present the performance measured in calibration and collision events.

2. Tile Calorimeter Read Out

The Tile Calorimeter [2] is required to measure particle energies in a dynamic range corresponding to 16 bits, extending from typical muon energy deposition of a few hundreds of MeV to the highest energetic jet of particles, which in rare cases can deposit up to two TeVs in a single cell. A scheme with a double readout using two independent 10-bit ADCs was chosen to cover this range. The PMT pulse is shaped, then fanned-out and amplified in two separate branches with a nominal gain ratio of 64 [3]. The two output pulses, referred to as high gain and low gain, have a fixed width (FWHM) of about 50 ns and an amplitude that is proportional to the energy deposited in the cell. The two pulses are digitized simultaneously by two ADCs at 40 Msps; the time series (samples) for each pulse is stored in the Data Management Unit [4] that also performs some first processing. Each pulse is sampled seven times in physics mode; up to nine samples may be recorded for calibration purposes. The high gain ADC is normally used unless the time series contain measurements which saturate the ADC. In this case the low ADC readout is used. The samples are kept in digital pipelines on the detector, and if the event is accepted by the LVL1 Trigger system, are sent to the back-end electronics, the Read Out Driver boards (ROD) [11]. Each ROD (see figure 1) receives data from eight calorimeter modules through optical links and synchronizes the data so that all the event fragments are
associated with the LHC bunch crossing (BCID) selected by the LVL1 trigger. Digital Signal Processors (DSP) are used for the implementation of the reconstruction algorithms, as described below. After reconstruction the event fragments are partially assembled and sent to the Read Out Buffers (ROBIn) for further processing by the Second Level Trigger.

Figure 1. Scheme of the Read Out Driver data-flow.

3. Optimal Filtering

Figure 2 shows an analog signal pulse and the ADC measurement samples, and illustrates the main characteristics of the pulse: amplitude, arrival phase and baseline level, or pedestal. The LHC is a synchrotron, the phase of the calorimeter signals of interaction events is expected to be synchronized with the LHC clock and constant within very small fluctuations. The residual fluctuations are mainly due to the longitudinal spread of proton bunches. The ADC measurement phase can be adjusted to compensate for delays and particle time of flight. In this condition the pulse time dependence can be linearized with a good approximation and the signal reconstructed with linear techniques [5]. The Optimal Filtering method have been chosen for the expected performance and its simplicity [6]. The algorithm extracts the three parameters of the shaped signal: the amplitude $A$, the phase $\tau$ and the baseline level $p$ using linear combinations of the samples $S_i$ with a set of weights $a_i, b_i$ and $c_i$:

$$A = \sum_{i=1}^{n} a_i S_i , \quad A\tau = \sum_{i=1}^{n} b_i S_i \quad \text{and} \quad p = \sum_{i=1}^{n} c_i S_i ,$$

(1)

where $n$ is the total number of samples. The weights are obtained minimizing the variance of the parameters against the electronic noise and Minimum Bias (MB) pileup fluctuations [6]. To give an example, the weights $a_i$, used in the amplitude computation are defined by the system of $n + 3$ equations:

$$\sum_{i=1}^{n} a_i g_i = 1 ,$$  
$$\sum_{i=1}^{n} a_i g'_i = 0 ,$$  
$$\sum_{i=1}^{n} a_i = 0 ,$$  
$$\sum_{j=1}^{n} a_j R_{ij} - \lambda g_i - \kappa g'_i - \nu = 0 \quad \text{for} \quad i = 1, n .$$

(2)

where $g_i = g(t_i)$ is the known signal pulse function, $g'_i$ the pulse first derivative, $\lambda, \kappa, \nu$ are Lagrange multipliers and $R_{ij}$ is the noise autocorrelation matrix defined as:

$$R_{ij} = \frac{\sum (n_i - \langle n_i \rangle)(n_j - \langle n_j \rangle)}{\sqrt{\sum (n_i - \langle n_i \rangle)^2 \sum (n_j - \langle n_j \rangle)^2}} ,$$

(3)
here we indicate with \( n \) the samples recorded on the electronic noise or other fluctuation due to MB pileup. Two similar systems of \( n + 3 \) equations hold for the weights \( b_i \) and \( c_i \) used for the phase and pedestal computation.

Note that in equation 1 the baseline level is not subtracted from the samples, but the constraint \( \sum_{i=1}^{n} a_i = 0 \) guarantees that any constant added to the samples \( S_i \) will not contribute to the amplitude.

In order to flag possible reconstruction failures, a reconstruction quality factor (QF) is defined as the square sum of the residuals:

\[
Q_F = \sum_{i=1}^{n} \left[ S_i - \left( A g_i + A \tau g_i' + \text{ped} \right) \right]^2.
\] (4)

The pulse shape function \( g(t) \) used to define the weights and the QF, is measured from the data. A single pulse shape template is used to describe all the channels in the calorimeter since channel by channel differences were found to be not important [7]. Different pulse templates extracted at different amplitudes, when rescaled, show a slightly deformation of the pulse height in the tail region. The distortion is small (\( \approx 1\% \)) and proved to have a negligible effect on the reconstructed amplitude and time [8, 7]. The QF is more sensitive to this distortion and shows a clear increase with the amplitude.

**Figure 3.** Behavior of the weight \( a_4 \) as a function of phase [10].

**Figure 4.** Behavior of the weight \( b_4 \) as a function of phase [10].

### 4. Implementation

The weights \( a_i, b_i, c_i \), as defined above, depend on the phase used to sample the signals, as shown in figures 3 and 4. The timing of each detector channel was established using laser calibration and collisions events [9]. The measured offsets are stored in the database. Sets of weights are computed for all phases covering the necessary range in 0.1 ns steps.

To reconstruct asynchronous data (e.g. cosmic rays), or to avoid the use of a priori definition of phases, an iterative method can be used in the reconstruction. In this mode the equations 1 are initially evaluated with an arbitrary phase, and the successive selection of the weight is based on the result of the previous step. The iterative method is slower and more sensitive to noise fluctuations. It is worth noting that the sample acquisition window is larger than the design LHC proton bunches separation and iterative algorithm can pick up signals generated in bunch crossing different than the triggered one. For this reason the default method is the non-iterative
one and we seldom use the iterative method for purposes of detector commissioning. Due to the execution time limits, the maximum LVL1 rate sustainable using iterations is about 30 KHz, the non-iterative method is well within the LVL1 trigger rate time requirement.

All the parameters needed by the reconstruction algorithm, like weights, phases and calibration constants are downloaded into the ROD/DSPs at the configuration time. The reconstructed amplitude provided to the LVL2 trigger algorithms is calibrated to the calorimeter electromagnetic energy scale by applying channel based calibration factors in the DSP.

The DSP reconstruction is necessarily limited by use of fixed point arithmetic and the internal precision available to describe the weights and calibration factors. Since the division is a time consuming operation in the DSP the phase from equation 1 is computed using a look-up table with the energy reciprocal pre-defined and stored in the DSP memory. One other limitation is in the size of output data fragments [10]. The reconstruction results are packed in a 32-bit word for each channel:15 bits for the energy, 11 bits for the time and 4 bits for the quality factor. The remaining bits encode the gain and an overall channel reconstruction good/bad status. This will be discussed more in the next section.

**Figure 5.** Numerical precision of the energy reconstructed in the ROD/DSP in the HG range evaluated using collision data.

**Figure 6.** Numerical precision of the energy reconstructed in the ROD/DSP in the LG range evaluated using collision data.

5. Validation

The ROD can be configured to send out both the reconstructed quantities and the raw data samples. Due to the bandwidth of the output link, this configuration is sustainable only up to a LVL1 trigger rates of about 45 KHz. The raw data obtained in this way can be reconstructed using well tested offline algorithms and used to validate the DSP implementation, to study the reproducibility of the results and to fully commission the detector in the harsh environment of the LHC. When the ATLAS data taking rate increases, only a small fraction of the data will contain samples. Therefore data validation at the start is important.

The first step in the validation of the DSP results is to verify the consistency of the online and offline implementations. Figures 5 and 6 show the residuals between the energy reconstructed online by the DSP and the one reconstructed offline by an equivalent algorithm showing the loss of precision due to the DSP limitations discussed above. Note that the degradation of individual channels is slightly energy dependent. Since this error scales with the channel level calibration factors, a band is shown covering from the 99% to the worst case. The worst cases arise in few PMTs with abnormal high voltage settings. The response needs to be boosted by a large factor to compensate for the gain deficit. The maximum deviation is about 2 MeV in the high gain range. For comparison the electronic noise RMS level is about 30 MeV. The low gain
scale has a precision of about 50 MeV, fully adequate in the range where signals are larger than approximately 8 GeV.

Figure 7 shows the difference between the time reconstructed in the DSP and offline as a function of the signal amplitude. Pseudo data are used for this study: data samples are generated according to the expected pulse shape, using a special module that emulates the front end electronics and covers a wide range of phases and amplitudes. The ROD is interfaced with the module and reconstructs the data in the normal fashion. The precision in the reconstructed time depends on the energy and phase granularity used in the look-up table; the oscillations apparent in figure 7 are an artifact of this granularity. Figure 8 shows the same difference as a function of the phases of the pulse. The maximum rounding error is about 0.5 ns. The larger differences up to 3 ns arise for small amplitudes and very large phases (up to 60 ns). In these conditions the numerical precision is not an issue since the reconstructed time is highly inaccurate in any case. The linear approximation discussed in section 3 does not hold. To cross-check the DSP implementation, the fixed point arithmetic and the precision used in the DSP constants and weights can be emulated in the offline reconstruction. Identical results are obtained online and offline when the DSP emulation is used [12].

One important further step in the validation is to evaluate the linearity and the resolution of the online non-iterative algorithm with respect to the offline iterative methods. In this way we evaluate all uncertainties due to numerical precision, understanding and description of the detector response and timing and the assumptions described in section 2. These studies have just started, and we are not able yet to give fully quantitative results. Figure 9 shows the DSP reconstructed time as a function of the offline time reconstructed with iterative methods. The DSP shows a good linearity for phases within 10 ns around the expected mean time. For larger time the deviation from linearity starts becoming important. Figure 10 shows the relative error in the DSP reconstructed energy as a function of the phase. The maximum bias is about 1% for pulses arriving 3 ns from the expected time. If needed, the bias can be easily corrected online also after finalizing the understanding of the tails in the time distributions.

5.1. Handling of unexpected conditions

Failures in the reconstruction, or unexpected results, can trigger the conditional dumping of the raw data sample on a channel by channel basis in order to make the raw data available for further offline processing. Examples of these conditions are: ADC saturation, unexpected...
reconstructed time, bad quality of the reconstruction, etc. These conditions are defined by a programmable logic based on the comparison of the reconstructed quantities with thresholds and other external conditions.

**Figure 9.** Time reconstructed in the DSP and time reconstructed offline with iterative method

**Figure 10.** Bias in the DSP energy reconstruction as a function of the reconstructed time and the behavior of a second order correction.

6. Summary and Conclusions

The energy reconstruction performed online in the Read Out Drivers is an important component of the ATLAS high level trigger. The evaluation of the algorithm performance started before collisions, using calibration, cosmic ray and pseudo data. The first collision data at 900 GeV and at 7 TeV have provided an estimate of the performance of the algorithm. The DSP results can be used in the High level trigger selection. Since the LVL1 trigger rate is currently lower than the design value, it is possible to operate in a transparent mode without losing any information. These data can be recorded and made available for offline reprocessing. Future results based on increased statistics and better understanding of the data are expected.

References

[1] ATLAS Detector and Physics Performance: Technical Design Report, CERN-LHCC-99-014 (1999); CERN-LHCC-99-015 (1999).
[2] Atlas Tile Calorimeter: Technical Design Report, CERN-LHCC-98-015 (1998).
[3] K. Anderson et al. Design of the front-end analog electronics for the ATLAS Tile Calorimeter. NIM A, 551:469476, 2005.
[4] C. Bohm et al. Atlas TileCal digitizer test system and quality control. ATLAS Note, ATL-TILECAL-2004-009, 2004.
[5] W. E. Cleland and E. G. Stern. Signal processing considerations for liquid ionization calorimeters in a high rate environment. NIM A, 338:467497, 1994.
[6] E. Fullana et al. Optimal Filtering in the ATLAS Hadronic Tile Calorimeter. ATLAS Note, ATL-TILECAL-2005-001, 2005.
[7] T. Carli et al. Effect of Pulse-Shape Variations on the Energy Reconstruction in the ATLAS Tile Calorimeter. Atlas Internal Note, ATL-COM-TILECAL-2009-033, 2009.
[8] K. Anderson et al. Performance and Calibration of the TileCal Fast Readout Using the Charge Injection System. Atlas Internal Note, ATL-COM-TILECAL-2008-003, 2008.
[9] C. Clement et al. Time Calibration of the ATLAS Hadronic Tile Calorimeter using the Laser System. Atlas Note, ATL-TILECAL-PUB-2009-003, 2009.
[10] B. Salvachua et al. Online energy and phase reconstruction: commissioning phase of the ATLAS Tile Calorimeter. Atlas Note, ATL-TILECAL-2008-004, 2008.
[11] A. Valero et al., ATLAS TileCal read out driver production. JINST, vol.2, p.P05003, 2007.
[12] Compare with page 9,10,12 of the slides shown at the Conference.