Mixed state properties of superconducting MgB$_2$ single crystals

M. Zehetmayer, M. Eisterer, and H. W. Weber
Atom-Institut der Österreichischen Universitäten, A-1090 Vienna, Austria

J. Jun, S. M. Kazakov, and J. Karpinski
Solid State Physics Laboratory, ETH, CH-8093 Zürich, Switzerland

A. Wisniewski
Institute of Physics, Polish Academy of Sciences, PL-02-668 Warsaw, Poland

We report in this Letter on magnetization measurements on superconducting MgB$_2$ single crystals. We find $\mu_0 H^c_2(0) = 3.2$ T, $\mu_0 H^a_2(0) = 14.5$ T, $\gamma = 4.6$, $\mu_0 H_c(0) = 0.28$ T, and $\kappa(T_c) = 4.7$. The standard Ginzburg-Landau (GL) parameter and the anisotropy effects.

PACS numbers: 74.25.Ha, 74.60.Ec, 74.70.Ad

The recent discovery of superconductivity in MgB$_2$ has attracted a lot of attention. Especially the rather high transition temperature of nearly 40 K in such a simple compound is of interest for applications, but also for an analysis of the physical mechanism leading to superconductivity. Several experiments indicate a phonon mediated s-wave BCS mechanism. Different models are proposed to explain the particular properties of MgB$_2$. Their correctness has to be checked by experiments, but only a few results are available on single crystals. We report on measurements of the magnetic moment in superconducting MgB$_2$, i.e. $m_c$. The Ginzburg-Landau (GL) parameter and the anisotropy effects.

Several single crystals of MgB$_2$ were grown using high pressure cubic anvil apparatus. Details of the process will be published elsewhere. Two crystals (sample A: $a \times b \times c \cong 660 \times 570 \times 21 \, \mu m^3$; sample B: $a \times b \times c \cong 600 \times 384 \times 54 \, \mu m^3$) were investigated by magnetic methods. The transition temperature ($T_c$) of each sample was obtained from the ac-susceptibility measured in a 1 T quantum interference device (SQUID) magnetometer. Sample A shows an onset of $T_c$ at 38 K and a rather broad transition of about 1 K. A linear fit of $H^c_2$ vs. $T$ near $T_c$ indicates a "bulk transition temperature" of 37.5 K (see inset of fig. 1a). In sample B we find $T_c = 38.3$ K, $\Delta T_c = 0.3$ K and a "bulk $T_c$" of 38.2 K. A simple analysis of the slope of the magnetic moment after reversing the applied field demonstrates that the size of the domain, in which the supercurrents flow without impedance, is identical to the sample size. Furthermore, a comparison of the calculated and the measured magnetization in the Meissner regime indicates a superconducting volume fraction of about 100%. The further evaluation of the mixed state parameters did not show significant differences between these two crystals.

The measurements of the magnetic moment were carried out in the 1 T and in an 8 T (SHE) SQUID magnetometer (for details, cf. [15]). Fig. 1a shows the upper critical field of MgB$_2$ for applied fields $H_a || c$ ($H^c_2$) and $H_a || ab$ ($H^a_2$). $H^c_2(T)$ is determined either from the onset of the superconducting signal in the $m(T)$ curve ("$T_a(H_a)$") or from the disappearance of the superconducting signal in the $m(H_a)$ curve. The same results were obtained by both methods. $H^a_2$ could be evaluated directly only below 8 T ($T > 21$ K in this case). At lower temperatures the London theory for the reversible magnetic moment $m_r$, i.e. $m_r \propto \ln(H^c_2/H_a)$, was used for the sake of simplicity to extrapolate the experimental $m_r$ data to zero. The very small magnetic moment in higher fields and the logarithmic behavior lead to rather large uncertainties in the evaluation, which are indicated by error bars in fig. 1a.

To obtain $H^c_2(0)$, the data were fitted to the function $H^c_2(t) = H^c_2(0)(1 - t^\alpha)^{\beta}$ with $\mu_0 H^c_2(0) = 3.18$ T ($t = T/T_c$, $T_c$ denotes the bulk transition temperature; $\alpha$, $\beta$ and $H^c_2(0)$ are fit parameters). The initial slope of the upper critical field ($k = \mu_0 \partial H^c_2/\partial T|_{T_c}$) is found to be -0.112 T/K near $T_c$, thus $\mu_0 H^c_2(0)/(kT_c) = -0.75$. This is close to the weak coupling BCS result ($\simeq -0.73$ in the clean limit, -0.69 would correspond to the dirty limit [16]). $H^c_2(T)$ is not very sensitive to the coupling strength and the above result, -0.75, is actually close to that of the strong coupling superconductor Pb [17], of course without considering anisotropy effects [18]. If we apply the same procedure to $H_a || ab$, we obtain...
The upper critical field anisotropy $\gamma = H_{c2}^\parallel / H_{c2}^\perp$ is shown in Fig. 1b (full squares). It increases from about 1 near $T_c$ to 4.2 at 22 K, in qualitative agreement with previous results \cite{1, 11, 13}. The open squares refer to results from torque measurements taken in a 9 T (Quantum Design) PPMS system. In this case, the angular dependence of the reversible torque is fitted to the anisotropic London theory with three fit parameters $\gamma$, $H_{c2}^\parallel$, and $\lambda_{ab}$ (cf. \cite{21}). A comparison of the latter two parameters with results from the SQUID measurements shows the high reliability of the evaluation. Note that this method does not lead to the anisotropy of the upper critical field, but rather to that of the magnetic penetration depth ($\lambda$), which can, in general, deviate from $H_{c2}^\parallel / H_{c2}^\perp$. In MgB$_2$, both seem to be the same, at least for $T \leq 30$ K. The torque indicates a small increase of $\gamma$ from 4.3 at 20 K to about 4.5 at 5 K leading to $\gamma(0) \approx 4.55$. However, we cannot exclude some small systematic errors in the evaluation, because (i) most of the recorded torque data refer to the irreversible regime. Therefore, the reversible signal ($\tau$) has to be calculated from the irreversible branches at increasing ($\tau_+$) and decreasing ($\tau_-$) angles ($\tau = [\tau_+ + \tau_-]/2$). The difference between the two branches is rather small, but grows at lower temperatures. (ii) The angular dependence of the background signal varies with temperature and cannot be determined exactly from measurements without a sample. However, different data sets for the background do not change $\gamma$ at 5 K significantly. Furthermore, the torque data were evaluated at several magnetic fields (0.5 - 2 T), the differences in $\gamma$ were very small (2 %). Based on the excellent agreement between the SQUID and the torque data in the overlapping temperature range, we assume that $\lambda_{c}/\lambda_{ab} = H_{c2}^{ab}/H_{c2}^c$ for $T < 21$ K, which allows us to calculate $H_{c2}^{ab}$ in this temperature range (cf. the solid squares for $H_{c2}^{ab}$ at $T < 21$ K in fig. 1a). This leads to $H_{c2}^{ab}(0) = 14.5$ T.

The further mixed state parameters can be calculated from the London theory and some Ginzburg-Landau relations. For instance, the magnetic penetration depth in the planes ($\lambda_{ab}$) is obtained from $\partial M/\partial \ln(H_a) = \phi_0/(8\pi\lambda_{ab}^2)$ for $H_a || c$ ($M = m_e/volume$, $\phi_0 \approx 2.07 \times 10^{-15}$ Vs). Since sample A shows a reversible magnetization already at very small fields (cf. fig. 2a), $\lambda_{ab}$ can be evaluated in the whole temperature range from 5 K to $T_c$ (see fig. 3a). A fit of $\lambda_{ab}^2(t)$ leads to $\lambda_{ab}(0) = 82$ nm and shows that the temperature dependence lies in between the (clean limit) BCS \cite{21} and a typical strong coupling model \cite{17}. The deviation at lower temperatures indicates a smaller energy gap - to - $T_c$ ratio than according to the BCS theory, in agreement with other experiments (e.g. \cite{22, 23}), which can be explained by the two band (assuming a small and a large gap \cite{24}) as well as by the anisotropic gap model \cite{3}. Further work on more comprehensive calculations including material dependent parameters are currently under way. The penetration depth in $c$ - direction is obtained from $\lambda_c = \gamma \lambda_{ab}$, hence $\lambda_c(0) = 370$ nm. The evaluation of $\lambda_c$ from the $m(T)$ measurements for $H_a || ab$ confirms the anisotropy, but is affected
by comparatively large errors.

Further, the (GL) relation $\mu_0 H_{c2}^{ab} = \phi_0/(2\pi \xi_{ab}^2)$ gives access to the coherence length in the ab - plane $\xi_{ab}$ and in the c - direction $\xi_c = \xi_{ab}/\gamma$ (fig. 2c). Accordingly, $\xi_{ab}(0) = 10.2$ nm and $\xi_c(0) = 2.3$ nm.

The lower critical field $H_{c1}$ can be calculated from $\mu_0 H_{c1}^c = [\phi_0/(2\pi \delta \xi_{ab}^2)] \cdot [\ln(\delta \lambda_{ab}/\xi_{ab}) + 0.5] \cdot (x = c$ and $\delta = 1$ for $H_{c1}$ and $x = ab$ and $\delta = \gamma$ for $H_{c1}^{ab}$), leading to $\mu_0 H_{c1}^c(0) = 63$ mT and $\mu_0 H_{c1}^{ab}(0) = 22$ mT (fig. 2c). A direct experimental assessment of $H_{c1}$ is usually quite difficult, because only the penetration field $H_p$, i.e. the field, at which the first flux lines enter the sample, can be obtained, which depends on the sample geometry [27], the anisotropy and the pinning force. We determined $H_p$ from measurements of the trapped magnetic moment, i.e. by measuring the moment in zero field after successively applying higher external fields and searching for the first deviation from zero at $H_p$ [28]. This procedure is still influenced by a finite critical current density $J_c$ and by geometry effects. For example, $\mu_0 J_c \approx 4$ mT at 5 K (sample A) can be converted into $H_{c1}(H_p)$ for a rectangular sample geometry [28], which leads to $H_{c1}/H_p \approx 17.7$ for $\gamma = 4.5$, i.e. $\mu_0 H_{c1}(5 \text{ K}) \approx 70$ mT, but overestimates $H_{c1}$ because the critical current density is not taken into account, and is not too far away from the calculated result of fig. 2: (62 mT at 5 K).

Furthermore, the thermodynamic critical field is calculated from the GL relation $\mu_0 H_c = \phi_0/(\sqrt{8\pi \lambda_{ab} c})$ and found to be 0.28 T at 0 K. Because $\Delta f = \mu_0 H_c^2/2$ (condensation energy), it can also be obtained by integrating the reversible magnetization $M(H_a)$, i.e. $\Delta f = \mu_0 H_a^2 c M dH_a$. The reversible magnetic moment is either calculated from the irreversible branches of the magnetization in increasing $(m_+)$ and decreasing $(m_-)$ fields in the fully penetrated state, $m_r = (m_+ + m_-)/2$ (cf. fig. 3) or directly measured. The results of the numerical integration are shown in fig. 2 and denoted by $H_{c1}[c]$ - direct and $H_{c1}[ab]$ - direct, respectively. A comparison with the GL results indicates that the London model for the magnetic penetration depth and the GL relations for $H_{c2}$ and $\xi$ represent excellent solutions for MgB$_2$. The maximum difference at low temperatures is less than 2 %.

To check the influence of uncertainties near $H_p$ in the direct evaluation (geometrical barrier, flux pinning), we replace $M(H_a)$ at 5 K by the separately measured Meissner slope at $0 \leq H_a \leq H_{c1}(1 - D)$ and by a simple logarithmic behavior at $H_{c1}(1 - D) \leq H_a \leq H_{c1}$, i.e. we simulate the behavior of an ellipsoidal sample, where the "effective demagnetization factor" $D$ is determined from $M(H_a) = -H_a/(1 - D)$ in the Meissner regime. This procedure reduces $H_c$ at 5 K and brings the above difference to almost zero.

The deviation function, $D(t) = [H_a(t)/H_a(0)] - [1 - t^2]$, describing the deviation of $H_c(t)$ from the parabolic behavior (two fluid model) and indicating the coupling strength in a conventional superconductor, is shown in
the inset of fig. 3. The maximum of -0.3 - 0.9 % lies in between the weak (≈ -3.5 %) and the strong coupling result (≈ +2.5 % for Pb). Although we have to consider evaluation errors, the results indicate a clear deviation from the weak coupling model, even if we consider the anisotropy (cf. [17]), and is consistent with other experiments (e.g. [16]).

The GL parameter $\kappa = \lambda/\xi$ is defined at $T = T_c$. At lower temperatures the Maki parameters [17] $\kappa_1 = H_{c2}/(\sqrt{H_c})$ and $\kappa_2 = [0.5 + 0.43/(\partial M/\partial H_a) H_{a,c} - 0.43D^2]^{1/2}$ can be used with $\kappa_1(T_c) = \kappa_2(T_c) = \kappa$. $\kappa_1$ (= $\lambda/\xi$ in the GL model) is shown in fig. 2 for $H_a/c$. Linear extrapolations lead to $\kappa_1(0) = 8.1$ and $\kappa_2(0) = 4.7$. The ratio $\kappa_1(0)/\kappa_1(T_c)$ is 1.72 and considerably larger than the BCS value (1.26 in the clean and 1.20 in the dirty limit [16]), but this is not unexpected considering stronger coupling [17] and anisotropy. $\kappa_2$ depends on the slope of $M$ near $H_{c2}$ and allows a precise determination of $\kappa^c$, which is again found to be 4.7 from a linear extrapolation to $T_c$. For $H_a||ab$, we get $\kappa_2^{ab}(0) = \gamma \kappa_1^c$ and therefore $\kappa_1^{ab}(0) = 37.1$ and $\kappa_2^{ab}(T_c) = 4.7$. The errors in $\kappa_2$ are relatively large in this case because of the very small slope of the magnetization near $H_{c2}$, but the extrapolation leads to $\kappa_2^{ab} = 5$, very close to $\kappa^c$.

At last, we turn to the irreversible properties of the MgB$_2$ single crystals. Hysteresis curves recorded at different temperatures are presented in fig. 3 for $H_a||c$ and $H_a||ab$. They demonstrate the excellent crystal quality by the small hysteresis and the low irreversibility fields in both directions. Note that all data points presented in fig. 3 were measured in the fully penetrated state. According to the Bean model [30] ($J_c$ is assumed to be constant), the critical current density in the planes can be calculated from the irreversible magnetic moment ($m_i = |m_+ - m_-|/2$). For rectangular samples we use $J_c(B) = |m_i(B)/\Omega| \{4/[b(1 - b/3a)]\}$ (sample volume: $\Omega = a \cdot b \cdot c$), and get $1.4 \times 10^8$ A m$^{-2}$ at 5 K in the remnant state for both samples. To obtain the irreversibility line, the onsets of a difference between the field cooled and the zero field cooled $m(T)$ measurement were evaluated. The results of fig. 3 (inset) show that the irreversibility line is very low for both field directions.

In summary, we presented measurements of the magnetic moments in single crystalline MgB$_2$ for fields $H_a||c$ and $H_a||ab$, and the subsequent evaluation of the basic mixed state parameters. The most important results are summarized in table I. The general consistency of the data set, which is documented nicely, e.g., by the results on the thermodynamic critical field, suggests that the standard theoretical description can be employed in MgB$_2$. The data indicate that MgB$_2$ is a low - $\kappa$ type II superconductor in the clean limit with an intermediate electron phonon coupling strength (cf. also [14, 15]), but a very large anisotropy.

We wish to thank F. M. Sauerzopf for useful discussions and H. Hartmann for technical assistance. This work was supported in part by the Austrian Science Foundation (FWF project 14422), the Austrian Exchange Service (OEAD 27/2000), the European Community (program ICA1-CT-2000-70018, Centre of Excellence CELDIS), the TMR Network SUPERCURRENT and the Swiss National Science Foundation.

*Electronic address: zehetm@at.ac.at

[1] J. Nagamatsu et al., Nature 410, 63 (2001).

[2] S. L. Bud’ko et al., Phys. Rev. Lett. 86, 1877 (2001).

[3] J.W. Quilty et al., Phys. Rev. Lett. 88, 087001 (2002).

[4] S. Haas and K. Maki, Phys. Rev. B 65, 205020 (2001).

[5] S.V. Shuliga et al., cond-mat/0103152 (unpublished).

[6] S. Lee et al., J. Phys. Soc. Jpn. 70, 2255 (2001).

[7] A. K. Pradhan et al., Phys. Rev. B 64, 212509 (2001).

[8] Yu. Eltsev et al., Phys. Rev. B 65, 140501(R) (2002).

[9] F. Manzano et al., Phys. Rev. Lett. 88, 047002 (2002).

[10] M. Angst et al., Phys. Rev. Lett. (to be published).

[11] A. V. Sologubenko et al., cond-mat/0112191 (unpublished).

[12] U. Welp et al., cond-mat/0203337 (unpublished).

[13] J. Karpinski et al. (unpublished).

[14] M. A. Angadi et al., Physica C 177, 479 (1991).

[15] F. M. Sauerzopf, Phys. Rev. B 57, 10959 (1998).

[16] E. Helfand and N. R. Werthamer, Phys. Rev. 147, 288 (1966).

[17] J. P. Carbotte, Rev. Mod. Phys. 62, 1027 (1990).

[18] W. Petschner and E. Schachinger, Phys. Rev. B 47, 3300 (1992).

[19] H. W. Weber et al., Phys. Rev. B 44, 7585 (1991).

[20] D. Zech et al., Phys. Rev. B 54, 12535 (1996).

[21] B. Mühlchlegel, Z. Phys. 155, 313 (1959).

[22] F. Giubileo et al., Phys. Rev. Lett. 87, 177008 (2001).

[23] P. Szabó et al., Phys. Rev. Lett. 87, 137005 (2001).

[24] F. Bouquet et al., Europhys. Lett. 56, 856 (2001).

[25] E. Zeldov et al., Phys. Rev. Lett. 73, 1428 (1994).

[26] C. Böhmer, G. Brandstätter, and H. W. Weber, Supercond. Sci. Technol. 10, A1 (1997).

[27] A. V. Kuznetsov, D. V. Eremenko, and V. N. Trofimov, Phys. Rev. B 56, 9064 (1997).

[28] T. B. Doyle, R. Labusch, and R. A. Doyle, Physica C 290, 148 (1997).

[29] K. Maki, Physics 1, 21 (1964).

[30] C. P. Bean, Phys. Rev. Lett. 8, 250 (1962).

[31] H. J. Choi et al., cond-mat/0111182 (unpublished).

[32] H. J. Choi et al., cond-mat/0111183 (unpublished).

| $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ | $\mu_0 H_{c2}(0)$ |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 3.18 T          | 14.5 T          | 38 K            | 0.28 T          | 63 mT           | 22 mT           | 47 mT           |
| $\lambda(0)$    | $\gamma(0)$    | $\gamma(0)$    | $\gamma(0)$    | $\gamma(0)$    | $\gamma(0)$    | $\gamma(0)$    |
| 370 nm          | 82 nm           | 4.6             | 4.6             | 2.3 nm         | 10.2 nm         | 1                |
| $\xi(0)$        | $\kappa(0)$    | $\kappa(0)$    | $\kappa(0)$    | $\kappa(0)$    | $\kappa(0)$    | $\kappa(0)$    |
| 8.1             | 37.1            | 4.7             | 4.7             | 8.1            | 37.1            | 4.7             |