Beam-Target Double Spin Asymmetry $A_{LT}$ in Charged Pion Production from Deep Inelastic Scattering on a Transversely Polarized $^3$He Target at $1.4 < Q^2 < 2.7$ GeV$^2$

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We report the first measurement of the double-spin asymmetry \( A_{LT} \) for charged pion electroproduction in semi-inclusive deep-inelastic electron scattering on a transversely polarized \(^3\)He target. The kinematics focused on the valence quark region, \( 0.16 < x < 0.35 \) with \( 1.4 < Q^2 < 2.7 \) GeV\(^2\). The corresponding neutron \( A_{LT} \) asymmetries were extracted from the measured \(^3\)He asymmetries and proton over \(^3\)He cross section ratios using the effective polarization approximation. These new data probe the transverse momentum dependent parton distribution function \( g_1^q \) and therefore provide access to quark spin-orbit correlations. Our results indicate a positive azimuthal asymmetry for \( \pi^- \) production on \(^3\)He and the neutron, while our \( \pi^+ \) asymmetries are consistent with zero.

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Understanding the spin structure of the nucleon in terms of parton spin and orbital angular momentum (OAM) remains a fundamental challenge in contemporary hadronic physics. The transverse momentum dependent (TMD) parton distribution functions (PDFs) [1, 2] describe the spin-correlated three-dimensional momentum structure of the nucleon’s quark constituents. Of the eight leading-twist TMD PDFs, five vanish after integration over quark’s transverse momentum, \( p_T \). Experimental information on these TMD PDFs is rather scarce. Among them, the transversal helicity \( g_1^q \) is a T-even and chiral-even distribution, which describes the \( p_T \)-correlated longitudinal polarization of quarks in a transversely polarized nucleon [1, 3]. Because \( g_1^q \) requires an interference between wave function components differing by one unit of quark OAM [4], the observation of a nonzero \( g_1^q \) would provide direct evidence that quarks carry orbital angular momentum, constraining an important part of the nucleon spin sum rule [5].

In recent years, semi-inclusive deep-inelastic lepton-nucleon scattering (SIDIS) and the Drell-Yan process have been recognized as clean experimental probes for TMD PDFs [6]. In the SIDIS process, \( \ell(l) + N(P) \rightarrow \ell'(l') + h(P_h) + X \), a lepton (\( \ell \)) scatters from a nucleon (\( N \)) and is detected in coincidence with a leading hadron (\( h \)) with particle four-momenta denoted by \( l, l', h \) and \( P_h \), respectively. All eight leading-twist TMD PDFs can be accessed using SIDIS [7]. In particular, the beam-helicity double-spin asymmetry (DSA) \( A_{LT} \) in SIDIS reactions on a transversely polarized nucleon is given at leading twist by

\[
A_{LT} (\phi_h, \phi_S) = \frac{1}{|P_BS_T|} \frac{Y^+ (\phi_h, \phi_S) - Y^- (\phi_h, \phi_S)}{Y^+ (\phi_h, \phi_S) + Y^- (\phi_h, \phi_S)} \sim A_{LT}^{\cos(\phi_h - \phi_S)} \cos (\phi_h - \phi_S),
\]

where \( \phi_h \) and \( \phi_S \) are the azimuthal angles of the produced hadron and the target spin as defined in the Trento convention [8], \( P_B \) is the polarization of the lepton beam, \( S_T \) is the transverse polarization of the target, and \( Y^\pm (\phi_h, \phi_S) \) is the normalized yield for beam helicity of \( \pm 1 \). The first and second subscripts to \( A \) denote the respective polarization of beam and target (L, T, and U represent longitudinal, transverse, and unpolarized, respectively). The partonic interpretation of the SIDIS cross section at the kinematic region of this experiment is supported by QCD factorization theory [9] and experimental data [10, 11]. At leading order (LO), the \( A_{LT}^{\cos(\phi_h - \phi_S)} \) asymmetry is proportional to the convolution of \( g_1^q \) and the unpolarized fragmentation function (FF) \( D_1 \) [3, 7].

Significant progress in theory and phenomenology regarding \( g_1^q \) and the related \( A_{LT}^{\cos(\phi_h - \phi_S)} \) asymmetry have been achieved in recent years. In a light-cone constituent quark model [12], \( g_1^q \) is explicitly decomposed into a dominant contribution from the interference of S- and P-waves and a minor (< 20%) contribution from the interference of P- and D-waves in the quark wavefunctions. The \( p_T^2 \)-moment of \( g_1^q \) can be estimated from the collinear \( g_1^q \) distribution function [13] using the Wandzura-Wilczek (WW)-type approximation [1, 3], which neglects the higher-twist contributions. In addition, the TMD PDFs have recently been explored in lattice QCD, using a simplified definition of the TMD PDFs with straight gauge links [14], \( g_1^q \) was among the first TMD PDFs addressed with this method. \( g_1^q \) has also been calculated in quark models as discussed in Refs. [15–22]. Common features of these models suggest that \( g_1^q \) is positive and \( g_1^q \) is negative. Both reach their maxima in the valence region at the few-percent level relative to the unpolarized distribution \( f_1^q \). The simple relation \( g_1^{\perp\perp} = -h_{1L}^{\perp\perp} \), where the \( h_{1L}^{\perp\perp} \) TMD PDF leads to the SIDIS \( A_{UL} \) asymmetry, has an essentially geometric origin and is supported by a large number of models [23]. Moreover, recent lattice QCD calculations indicate that the relation may indeed be approximately satisfied [14, 24]. In addition, the QCD parton model suggests approximate TMD relations, which link \( g_1^q \) with the quark transversity distribution \( h_1^T \) and the pretzelosity distribution, \( h_{1T}^{\perp\perp} \) [25]. \( A_{LT}^{\cos(\phi_h - \phi_S)} \) has been predicted for the kinematics and reaction channels of this experiment using the WW-type approximations [26, 27], a light-cone constituent quark model [12, 16], a diquark spectator model [20] and a light-cone quark-diquark model [21].

The COMPASS collaboration previously reported preliminary results for \( A_{LT}^{\cos(\phi_h - \phi_S)} \) in positive and negative charged hadron production using a muon beam scattered from transversely polarized deuterons [28] and protons [29]. The kinematics favored the sea quark region. Within the uncertainties, the preliminary results cannot differentiate between zero and various model predictions.
In this Letter, we report new results from experiment E06-010 in Jefferson Lab Hall A, which measured the $A_{LT}$ DSA and the target single spin asymmetries (target-SSA) \cite{30} in SIDIS reactions on a transversely polarized $^3\text{He}$ target. The experiment used a longitudinally polarized 5.9 GeV electron beam with an average current of 12 $\mu$A. Polarized electrons were excited from a superlattice GaAs photocathode by a circularly polarized laser \cite{31} at the injector of the CEBAF accelerator. The laser polarization, and therefore the electron beam-helicity, was flipped at 30 Hz using a Pockels cell. The average beam polarization was $(76.8 \pm 3.5)\%$, which was measured periodically by Möller polarimeter. Through an active feedback system \cite{32}, the beam charge asymmetry between the two helicity states was controlled to less than 150 ppm over a typical 20 min period between target spin-flips and less than 10 ppm for the entire experiment. In addition to the fast helicity flip, roughly half of the data were accumulated with a half-wave plate inserted in the path of the laser at the source, providing a passive helicity reversal for an independent cross-check of the systematic uncertainty.

The ground state $^3\text{He}$ wave function is dominated by the $S$ state, in which the two proton spins cancel and the nuclear spin resides entirely on the single neutron \cite{33}. Therefore, a polarized $^3\text{He}$ target is the optimal effective polarized neutron target. The target used in this measurement is polarized by spin-exchange optical pumping of a Rb-K mixture \cite{34}. A significant improvement in target polarization compared to previous experiments was achieved using spectrally narrowed pumping lasers \cite{35}, which improved the absorption efficiency. The $^3\text{He}$ gas of 10 atm pressure was contained in a 40-cm-long glass vessel, which provided an effective electron-polarized neutron luminosity of $10^{36} \text{cm}^{-2}\text{s}^{-1}$. The beam charge was divided equally among two target spin orientations transverse to the beamline, parallel and perpendicular to the central $\vec{L}\bar{P}$ scattering plane. Within each orientation, the spin direction of the $^3\text{He}$ was flipped every 20 min through adiabatic fast passage \cite{36}. The average in-beam polarization was $(55.4 \pm 2.8)\%$ and was measured during each spin flip using nuclear magnetic resonance, which in turn was calibrated regularly using electron paramagnetic resonance \cite{37}.

The scattered electron was detected in the BigBite spectrometer, which consisted of a single dipole magnet for momentum analysis, three multirife drift chambers for tracking, a scintillator plane for time-of-flight measurement and a lead-glass calorimeter divided into preshower and shower sections for electron identification (ID) and triggering. Its angular acceptance was about $64 \text{msr}$ for a momentum range from 0.6 to 2.5 GeV. The left high resolution spectrometer (HRS) \cite{38} was used to detect hadrons in coincidence with the BigBite spectrometer. Its detector package included two drift chambers for tracking, two scintillator planes for timing and triggering, a gas Cerenkov detector and a lead-glass shower detector for electron ID. In addition, an aerogel Cerenkov detector and a ring imaging Čerenkov detector were used for hadron ID. The HRS central momentum was fixed at 2.35 GeV with a momentum acceptance of $\pm 4.5\%$ and an angular acceptance of $\sim 6 \text{msr}$.

The SIDIS event sample was selected with particle identification and kinematic cuts, including the four momentum transfer squared $Q^2 > 1 \text{GeV}^2$, the virtual-photon-nucleon invariant mass $W > 2.3 \text{GeV}$, and the mass of undetected final-state particles $W' > 1.6 \text{GeV}$. The kinematic coverage was in the valence quark region for values of the Bjorken scaling variable in $0.16 < x < 0.35$ at a scale of $1.4 < Q^2 < 2.7 \text{GeV}^2$. The range of measured hadron transverse momentum $P_{h\perp}$ was 0.24-0.44 GeV. The fraction $z$ of the energy transfer carried by the observed hadron was confined by the HRS momentum acceptance to a small range about $z \sim 0.5-0.6$. Events were divided into four $x$ bins with equivalent statistics. At high $x$, the azimuthal acceptance in $\phi_h - \phi_S$ was close to $2\pi$, while at lower $x$, roughly half of the $2\pi$ range was covered, including the regions of maximal and minimal sensitivity to $A_{LT}^{\cos(\phi_h - \phi_S)}$ at $\cos(\phi_h - \phi_S) \sim \pm 1$ and zero, respectively. The central kinematics were presented in Ref. \cite{30}.

The beam-helicity DSA was formed from the measured yields as in Eq. (1). The azimuthal asymmetry in each $x$-bin was extracted directly using an azimuthally unbinned maximum likelihood estimator with corrections for the accumulated beam charge, the data acquisition live time, and the beam and target polarizations. The result was confirmed by an independent binning-and-fitting procedure \cite{30}. The sign of the asymmetry was cross-checked with that of the known asymmetry of $^3\text{He}(e',e')$ elastic and quasielastic scattering on longitudinally and transversely polarized targets \cite{39}. The

![Figure 1](image-url)
small amount of unpolarized N\textsubscript{2} used in the target cell to reduce depolarization diluted the measured \(^3\text{He}\) asymmetry, which was corrected for the nitrogen dilution defined as

\[
f_{N_2} = \frac{N_{N_2} \sigma_{N_2}}{N_{\text{He}} \sigma_{\text{He}} + N_{N_2} \sigma_{N_2}},
\]

where \(N\) is the density and \(\sigma\) is the unpolarized SIDIS cross section. The ratio \(\sigma_{\text{He}}/\sigma_{N_2}\) was measured periodically in dedicated runs on targets filled with known amounts of pure unpolarized \(^3\text{He}\) and N\textsubscript{2}, resulting \(f_{N_2} \sim 10\%\). A 5%-20% longitudinal component of the target polarization with respect to the virtual-photon direction introduced a small correction to \(A_{LT}(\phi_h, \phi_S)\) from the DSA \(A_{UL}\). \(A_{LL}\) and its uncertainty were calculated from the results of the DSSV 2008 global fit [13] combined with \(P_{h\perp}\) dependence from a fit to recent proton data [40].

The \(A_{UL}\) uncertainty also includes a contribution from the longitudinal virtual-photon cross section, which was calculated using the SLAC-R1999 parametrization [41]. The \(A_{LT}\) results for \(^3\text{He}\) and the \(A_{LL}\) correction applied to the data are shown in Fig. 1. Combining the data from all four \(x\)-bins, we have observed a positive asymmetry with 2.8 \(\sigma\) significance for \(\pi^-\) production on \(^3\text{He}\), while the \(\pi^+\) asymmetries are consistent with zero.

The systematic uncertainties in our measurements due to acceptance, detector response drift and target density fluctuations were suppressed to a negligible level by the fast beam-helicity reversal. With the addition of the frequent target spin reversal, the contributions from the beam-SSA \(A_{LU}\) and the target-SSA \(A_{LT}\) were canceled in the extraction of \(A_{LT}^{\cos(\phi_h - \phi_S)}\). The dominant systematic effect for the lower \(x\)-bins was the contamination from photon induced charge-symmetric \(e^\pm\) pair production, in which the \(e^-\) was detected in the BigBite spectrometer. The yield of \((e^+, \pi^\pm)\) coincidences was measured by reversing the magnetic field of the BigBite spectrometer [30]. Since the measured asymmetry of the background was consistent with zero, the contamination was treated as a dilution. Bin centering \(|\delta A_{LT}/A_{LT}| \leq 14\%\) and radiative \(|\delta A_{LT}| \leq 0.1\%\) effects were estimated with an adapted SIMC Monte Carlo simulation [11] and POLRAD2 [42]. Other noticeable systematic uncertainties include the \(\pi^-\) contamination in the electron sample from the BigBite spectrometer \(|\delta A_{LT}| \leq 0.1\%\), the kaon contamination in the pion sample from the HRS \(|\delta A_{LT} | \leq 0.1\%\), and the beam and target polarimetry \(|\delta A_{LT}/A_{LT}| \leq 5\%, each\). Finally, uncertainties in the Cahn \(A_{UU}^{\cos(\phi_h + \phi_S)}\) and Boer-Mulders \(A_{UU}^{\cos(2\phi_h)}\) effects on the unpolarized cross section [6] induce relative systematic uncertainties \(|\delta A_{LT}/A_{LT}| \leq 10\%\) and 5\%, respectively. The contamination in identified SIDIS events from decays of diffractively produced \(\rho\) mesons, estimated to range from 3%-5\% (5%-10\%) for \(\pi^+\) (\(\pi^-\)) by PYTHIA6.4 [43], was not corrected, consistent with previous experimental analyses [30, 40, 44, 45]. Experimental information regarding the subleading-twist \(\cos(\phi_h - \phi_S)\) and \(\cos(2\phi_h - \phi_S)\) moments of \(A_{LT}\) is rather scarce. However, existing evidence for the suppression of subleading-twist effects in other observables of inclusive and semi-inclusive DIS in the kinematic region of this experiment [11, 46, 47] supports the leading-twist interpretation presented in this Letter. Therefore, the potential systematic effect of these terms on the extraction of the leading-twist \(\cos(\phi_h - \phi_S)\) moment is expected to be small compared to the statistical uncertainties of the present data, and is not included in the quoted systematic uncertainty. Future high-precision SIDIS data covering a broader \(Q^2\) range will enable an accurate determination of the subleading-twist \(A_{LT}\) moments [48, 49].

The neutron asymmetry was extracted from the \(^3\text{He}\) asymmetry using the effective polarization approximation, given by

\[
A_{LT}(\phi_h, \phi_S) = \frac{1}{(1 - f_p) P_n} \left( A_{LT}^{\text{He}} - f_p A_{LT}^{\text{P}} P_p \right),
\]

where the proton dilution factor \(f_p \equiv 2 \sigma_p/\sigma_{\text{He}}\) was measured with unpolarized \(^3\text{He}\) and hydrogen gas targets in identical kinematics, including the uncertainties from spin-independent final-state interactions (FSI) [30]. The effective neutron and proton polarizations in \(^3\text{He}\) are given by \(P_n = 0.86^{+0.036}_{-0.028}\) and \(P_p = -0.028^{+0.004}_{-0.009}\) [50], respectively. Because of the small proton polarization and a scarcity of existing data, no \(A_{LT}^{\text{P}}\) correction was applied to our results. The allowed range of \(A_{LT}^{\text{P}}\) was estimated from COMPASS data [29], which resulted in a systematic uncertainty in \(A_{LT}^{\text{P}}\) of less than 30% of the statistical uncertainty. Target single-spin-dependent FSI effects on the DSA were canceled by the frequent target spin flips, resulting in negligible uncertainty in the extracted \(A_{LT}\).

The results are shown in Fig. 2 and are compared to several model calculations, including WW-type approximations with parametrizations from Ref. [26] and Ref. [26, 27], a light-cone constituent quark model (LCCQM) [12, 16] and a light-cone quark-diquark
model (LCQDM) evaluated using approach two in Ref. [21]. While the extracted $A_{LT}^q(\pi^\pm)$ is consistent with zero within the uncertainties, $A_{LT}^n(\pi^-)$ is consistent in sign with these model predictions but favors a larger magnitude. Sizable asymmetries could be expected for future experiments, including corresponding SIDIS asymmetries on a proton target and the double-polarized asymmetry in Drell-Yan dilepton production. While the $\pi^+$ and $\pi^-$ data are consistent with the interplay between S-P and P-D wave interference terms predicted by the LCCQM and LCQDM models, the magnitude of the measured $\pi^-$ asymmetry suggests a larger total contribution from such terms than that found in the LCCQM. The larger magnitude of the data compared to the WW-type calculations suggests either a different $P_{h,\perp}$ dependence of $A_{LT}$ than assumed in the calculations, a significant role for subleading-twist effects, or both. The statistical precision and kinematic coverage of the present data cannot distinguish between these scenarios. It is worth noting that the sign of $A_{LT}^n(\pi^-)$ is opposite to the sign of the $A_{LT}^{\sin 2\phi_h}$ asymmetry in $\pi^+$ production on the proton measured by the CLAS collaboration [40]. This observation is consistent with many models which support that $g_{1T}^n$ and $h_{1T}^{\pm^*}$ have opposite signs [23].

In conclusion, we have reported the first measurement of the DSA $A_{LT}^{\cos(\phi_h - \phi_S)}$ in SIDIS using a polarized electron beam on a transversely polarized $^3$He target. The neutron $A_{LT}$ was also extracted for the first time using the effective polarization approximation. Systematic uncertainties were minimized by forming the raw asymmetry between beam-helicity states with minimal charge asymmetry due to the fast helicity reversal. A positive asymmetry was observed for $^3$He $(e, e'\pi^-) X$ and $^6$Li $(e, e'\pi^-) X$, providing the first experimental indication of a nonzero $A_{LT}$, which at leading twist leads to a nonzero $g_{1T}^n$. When combined with measurements on proton and deuteron targets, these new data will aid the flavor-decomposition of the $g_{1T}^n$ TMD PDF. This work has laid the foundation for the future high-precision mapping of $A_{LT}$ following the JLab 12 GeV upgrade [48] and at an electron-ion collider [49], which will provide a comprehensive understanding of the $g_{1T}^n$ TMD PDF and the subleading-twist effects.

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[1] P. J. Mulders and R. D. Tangerman, Nucl. Phys. B461, 197 (1996).
[2] D. Boer and P. J. Mulders, Phys. Rev. D57, 5780 (1998).
[3] A. M. Kotzinian and P. J. Mulders, Phys. Rev. D54, 1229 (1996).
[4] X.-D. Ji, J.-P. Ma, and F. Yuan, Nucl. Phys. B652, 383 (2003).
[5] R. Jaffe and A. Manohar, Nucl. Phys. B337, 509 (1990).
[6] V. Barone, F. Bradamante, and A. Martin, Prog. Part. Nucl. Phys. 65, 267 (2010).
[7] A. Bacchetta et al., JHEP 02, 093 (2007).
[8] A. Bacchetta, U. D’Alesio, M. Diehl, and C. A. Miller, Phys. Rev. D70, 117504 (2004).
[9] X.-D. Ji, J.-p. Ma, and F. Yuan, Phys. Rev. D71, 034005 (2005).
[10] H. Avakian et al. (CLAS), Phys. Rev. D69, 112004 (2004).
[11] R. Asaturyan et al., Phys. Rev. C 85, 015202 (2012).
[12] S. Boffi, A. V. Efremov, B. Pasquini, and P. Schweitzer, Phys. Rev. D79, 094012 (2009).
[13] D. de Florian, R. Sassot, M. Stratmann, and W. Vogelsang, Phys. Rev. Lett. 101, 072001 (2008).
[14] P. Hagler et al., Europhys. Lett. 88, 61001 (2009).
[15] R. Jakob, P. Mulders, and J. Rodrigues, Nucl. Phys. A626, 937 (1997).
[16] B. Pasquini, S. Cazzaniga, and S. Boffi, Phys. Rev. D78, 034025 (2008).
[17] A. Kotzinian, arXiv:0806.3804 [hep-ph].
[18] A. V. Efremov, P. Schweitzer, O. V. Teryaev, and P. Zavada, Phys. Rev. D80, 014021 (2009).
[19] H. Avakian, A. V. Efremov, P. Schweitzer, and F. Yuan, Phys. Rev. D81, 074035 (2010).
[20] A. Bacchetta et al., Eur. Phys. J. A45, 373 (2010).
[21] J. Zhu and B.-Q. Ma, Phys. Lett. B696, 246 (2011).
[22] A. V. Efremov et al., J. Phys. Conf. Ser. 295, 012052 (2011).
[23] C. Lorce and B. Pasquini, arXiv:1104.5651 [hep-ph].
[24] B. U. Musch, P. Hagler, J. W. Negele, and A. Schafer, Phys. Rev. D83, 094507 (2011).
[25] E. Di Salvo, Mod. Phys. Lett. A22, 1787 (2007).
[26] A. Kotzinian, B. Parsamyan, and A. Prokudin, Phys. Rev. D73, 114017 (2006).
[27] A. Prokudin, (private communication).
[28] B. Parsamyan (COMPASS), Eur. Phys. J. ST 162, 89 (2008).
[29] X. Qian et al. (The Jefferson Lab Hall A), Phys. Rev. Lett. 107, 072003 (2011).
[30] C. Sinclair et al., Phys. Rev. ST Accel. Beams 10, 023501 (2007).
[31] D. Androic et al. (G0), Nucl. Instrum. Meth. A646, 59 (2011).
[32] F. P. Bissey, V. A. Guzey, M. Strikman, and A. W. Thomas, Phys. Rev. C65, 064317 (2002).
[33] E. Babcock et al., Phys. Rev. Lett. 91, 123003 (2003).
[34] J. Singh et al., AIP Conf. Proc. 1149, 823 (2009).
[35] A. Abragam, Principles of Nuclear Magnetism (Oxford University, New York, 1961).
[36] M. V. Romalis and G. D. Cates, Phys. Rev. A 58, 3004 (1998).
[37] J. Alcorn et al., Nucl. Instrum. Meth. A522, 294 (2004).
[38] T. Donnelly and A. Raskin, Annals Phys. 169, 247 (1986).
[39] H. Avakian et al. (CLAS), Phys. Rev. Lett. 105, 262002
Table I. Central kinematics and asymmetry results. The format for $^3$He and neutron $A_{LT}^{\cos(\phi_h - \phi_S)}$ asymmetries follows “central value” ± “statistical uncertainty” ± “systematic uncertainty”.

| $x$ | $Q^2$ GeV$^2$ | $y$ | $z$ | $P_{h\perp}$ GeV | $^3$He $A_{LT}^{\cos(\phi_h - \phi_S)}$ | $^3$He $A_{LT}^{\cos(\phi_h - \phi_S)}$ | neutron $A_{LT}^{\cos(\phi_h - \phi_S)}$ | neutron $A_{LT}^{\cos(\phi_h - \phi_S)}$ |
|-----|--------------|-----|-----|------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|
| 0.156 | 1.38          | 0.81 | 0.50 | 0.43            | +0.003 ± 0.020 ± 0.004       | +0.030 ± 0.020 ± 0.008       | +0.02 ± 0.11 ± 0.03       | +0.10 ± 0.07 ± 0.03       |
| 0.206 | 1.76          | 0.78 | 0.52 | 0.38            | +0.005 ± 0.016 ± 0.004       | +0.032 ± 0.019 ± 0.007       | +0.04 ± 0.13 ± 0.06       | +0.18 ± 0.11 ± 0.06       |
| 0.265 | 2.16          | 0.75 | 0.54 | 0.32            | −0.019 ± 0.015 ± 0.004       | +0.024 ± 0.017 ± 0.004       | −0.13 ± 0.11 ± 0.05       | −0.10 ± 0.07 ± 0.02       |
| 0.349 | 2.68          | 0.70 | 0.58 | 0.24            | −0.025 ± 0.015 ± 0.005       | +0.034 ± 0.017 ± 0.006       | −0.27 ± 0.18 ± 0.13       | −0.18 ± 0.10 ± 0.05       |

(2010).
[41] K. Abe et al. (E143 Collaboration), Phys. Lett. B452, 194 (1999).
[42] I. Akushevich et al., Comput. Phys. Commun. 104, 201 (1997).
[43] T. Sjostrand, S. Mrenna, and P. Z. Skands, JHEP 0605, 026 (2006).
[44] A. Airapetian et al. (HERMES), Phys. Rev. Lett. 103, 152002 (2009).
[45] A. Airapetian et al. (HERMES), Phys. Lett. B693, 11 (2010).
[46] E. Leader, A. V. Sidorov, and D. B. Stamenov, Phys. Rev. D75, 074027 (2007).
[47] J. Blumlein and H. Bottcher, Nucl. Phys. B841, 205 (2010).
[48] H. Gao et al., Eur.Phys.J.Plus 126, 2 (2011).
[49] M. Anselmino et al., Eur. Phys. J. A47, 35 (2011).
[50] X. Zheng et al. (Jefferson Lab Hall A Collaboration), Phys. Rev. Lett. 92, 012004 (2004).