Higgs production via gluon fusion from $k_T$-factorisation

F. Hautmann*, H. Jung† and V. Pandis**

*Theoretical Physics Department, University of Oxford, Oxford OX1 3NP, UK
†Deutsches Elektronen Synchrotron, Hamburg 22603, Germany
**Department of Applied Mathematics and Theoretical Physics, Cambridge, CB3 0WA, UK

Abstract. Theoretical studies of Higgs production via gluon fusion are frequently carried out in the limit where the top quark mass is much larger than the Higgs mass, an approximation which reduces the top quark loop to an effective vertex. We present a numerical analysis of the error thus introduced by performing a Monte Carlo calculation for $gg \to h$ in $k_T$-factorisation, using the parton shower generator CASCADE. We proceed to compare CASCADE to the collinear Monte Carlos PYTHIA, MC@NLO and POWHEG. We study the dependence of parton radiation on the resummation of high-energy corrections taken into account by $k_T$-factorisation, and its influence on predictions for the Higgs $p_T$ spectrum.

Keywords: Higgs, Monte Carlo, $k_T$-factorisation, Gluon Fusion
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INTRODUCTION

In the $k_T$-factorisation method [1–4] one makes the transition from parton-level to hadron-level cross-sections through a convolution with the unintegrated parton distribution functions [5, 6]. By retaining the dependence on the transverse momenta and evaluating the cross-section with off-shell incoming partons, the potentially large high-energy logarithms are automatically resummed.

Higgs boson production via gluon fusion is mediated through a top quark loop. In the heavy-top limit in which $2m_t/m_H \gg 1$ this loop can be replaced by an effective vertex, reducing the loop count by one and simplifying the calculation [7]. This approximation is frequently used in theoretical studies of the Higgs so a quantification of the error introduced is important. Numerical analyses in collinear factorisation indicate that the effects of the top-mass are small when $2m_t/m_H < 1$ [8–10].

The cross-section of the top-quark triangle with off-shell initial-state gluons, having first been derived in the heavy-top limit [11, 12], now exists in the literature with the full $m_t$ dependence [13, 14]. It is therefore possible to examine the impact of this approximation on both inclusive and exclusive quantities, now within $k_T$-factorisation. A comparison of the cross-sections was carried out in Ref. [13, 15] concluding that on the inclusive level corrections are of the order of 5%. Through the use of the $k_T$-factorised Monte Carlo CASCADE [16, 17] we confirm this finding and extend the investigation to the spectrum of the mini-jet radiation accompanying the Higgs.

An additional question, conceptually separate from the heavy-top approximation, is the dependence of gluon radiation in association with Higgs production on the resumma-
FIGURE 1. The quantity $1 - \frac{d\sigma(m_{top} \rightarrow \infty)}{dW} / \frac{d\sigma(m_{top})}{dW}$ is plotted for $W = p_T^{Higgs}$ (left) and $W = y^{Higgs}$ (right), where $y$ is the rapidity. The error bars reflect only the statistical error of the Monte Carlo. These plots were obtained using the CCFM Set A [16, 22].

...tion of high energy corrections. We examine the impact of extra gluon radiation on the Higgs $p_T$ spectrum by comparing CASCADE to the collinearly-factorised PYTHIA [18], MC@NLO [19] and POWHEG [20, 21].

All plots have been obtained for $pp$ collisions at $\sqrt{s} = 14$ TeV and $m_H = 120$ GeV.

EFFECTS OF THE FINITE TOP-QUARK MASS

We find that retaining the full top-mass dependence in the matrix element leads to a small and approximately uniform increase in the differential cross-sections in $p_T$ and $y$ of the order of 5%. This is illustrated in Fig. 1 and is consistent with previous studies [13, 15].

We extend the study of top-mass effects by examining the mini-jet activity accompanying Higgs boson production. We follow the underlying event analyses of Ref. [23, 24], to which the reader is referred for the basic approach and motivation. We divide the azimuthal plane in four regions and accordingly classify the jets produced in association with the Higgs. Jets are defined using the SISCone algorithm [25] of the FastJet [26] package with $R = 0.4$ and $f = 0.5$, applied on the hadron level. We impose the cut $p_T^{jet} > 10$ GeV. The resulting multiplicity distributions in the four azimuthal regions are shown in Fig. 2, plotted against the Higgs transverse momentum. They appear to not be very sensitive to mass effects in the matrix element.

COMPARISON TO COLLINEAR MONTE CARLOS

We compare the effect of resumming higher-order contributions with a purely collinear description of radiation. We extend the analysis of Ref. [23] where CASCADE was compared to the LO$^1$ Monte Carlo PYTHIA to include the collinear NLO generators MC@NLO and POWHEG. Showering in MC@NLO is performed through the angular-ordered HERWIG [27, 28] and we run POWHEG coupled to the PYTHIA shower. We operate PYTHIA with the ‘new’ underlying event model [29, 30] (PYENVW) using the

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$^1$ PYTHIA also implements partial radiative higher-order corrections.
FIGURE 2. The ratio $1 - \frac{dN(m_{W^\pm} \to \infty)}{dp_T} / \frac{dN(m_{W^\pm})}{dp_T}$ is shown, where $N$ the number of mini-jets. The histograms are normalised to the $p_T$ spectrum of the Higgs and thus do not scale with the cross-section.

FIGURE 3. The $p_T$ (left) and rapidity (right) spectrum of the Higgs. The curves have been scaled to a common token cross-section of 1 pb.

‘Perugia 0’ tune [31].

In order to make a baseline comparison with the collinear Monte Carlos we take the on-shell approximation for the hard matrix element $\text{ME}(k_T) \to \text{ME}(k_T = 0) \theta(\mu - k_T)$, where $\mu$ is the factorisation scale. We use unintegrated gluon distributions obtained from deconvolution of the ordinary distributions as described in Ref. [1]. We use one such standard set implemented in CASCADE [16, 17]. For the collinear generators we used the CTEQ6M [32] set. The results are plotted in Fig. 3.

Additional corrections to the matrix element associated with the off-shellness contribute significantly to the spectrum. The details of this will be elaborated on in a forthcoming publication. We find that the details of the initial-state showering are important even in the high-$p_T$ region.

CONCLUSION

We have implemented top-mass terms in the $k_T$-factorised Monte Carlo CASCADE. We have used this to analyse the uncertainty induced by the heavy-top approximation that
is commonly used to simplify loop calculations. We have investigated this both for the inclusive cross-section and the multiplicity of mini-jets accompanying the Higgs boson. Furthermore, we have examined the effect of the higher-order radiative terms re-summed by $k_T$-factorisation on the Higgs $p_T$ spectrum. We have compared CASCADE with the collinear Monte Carlos PYTHIA, POWHEG and MC@NLO. We find that the impact of both the unintegrated gluon distributions and matrix elements is significant even at $p_T$ of the order or higher than the Higgs mass.

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