Introduction. The search for Majorana zero energy modes which obey non-Abelian statistics has been one of the most exciting areas of research in the past decade [1,2]. It was first proposed that two-dimensional $p + ip$-wave superconductors support chiral Majorana edge states [3–5], while one-dimensional $p$-wave superconductors support localized Majorana zero energy modes at the ends of the superconductors [6]. Several experimentally promising schemes to engineer effective $p + ip$ topological superconductors which support Majorana modes have been proposed [7,8]. First, Fu and Kane showed that the vortex cores of superconducting surface states of topological insulators host Majorana fermions [7]. Spin-dependent zero-bias conductance peaks possibly associated with Majorana fermion in superconducting topological superconductors have been observed [8,9]. Second, it was also suggested that Majorana modes can exist as end states of semiconductor wires in proximity to superconductors [10–12]. Zero-bias conductance peaks have been reported as signatures of Majorana fermions in these semiconductor-wire/superconductor heterostructures [13–15]. More recently, the observation of the predicted $2e^2/h$ conductance peak [16,17] provides strong evidence that Majorana fermions have been observed in this system [18,19]. However, it remains challenging to engineer scalable Majorana networks based on the semiconductor schemes [20].

A recent paper reported the realization of the effective $p + ip$ wave superconductor with chiral Majorana edge states in quantum anomalous Hall/superconductor (QAH/SC) heterostructures, based on the observation of half-quantized conductance plateaus in two-terminal transport experiments [21] as predicted previously [22–24]. Unfortunately, chiral Majorana modes, being extended, cannot be used for topological quantum computation. Here, we suggest using quasi-one-dimensional (quasi-1D) QAH/SC heterostructures to realize localized Majorana zero energy modes. Importantly, the topological regime of this geometry is much larger than the two-dimensional chiral topological superconducting case, which requires the superconducting pairing gap to be larger than the bulk gap of the QAH system. Moreover, the experimental parameters of Cr or V doped (Bi,Sb)$_2$Te$_3$ QAH thin films are highly tunable by external magnetic fields and gating [25–32], and complicated device geometry can be achieved by standard fabrication techniques. Therefore, the system provides a promising platform for braiding Majorana zero energy modes and scalable quantum computations [20,33].

In the following sections, we first demonstrate that quasi-1D QAH systems in proximity to an s-wave superconductor exhibits a large, experimentally accessible, topological regime, which supports localized Majorana zero energy modes. When the quasi-1D QAH system is narrow compared with the localization length of the edge modes, the two chiral edge modes of QAH are coupled to form a single helical conducting channel as shown in Fig. 1. When superconductivity is induced on this single conducting channel, an effective $p$-wave superconductor is realized similar to the Rashba semiconductor wire systems proposed previously [10–12]. Importantly, the edge modes in quasi-1D QAH are well separated from the bulk states, giving rise to a topological regime of about 10 meV which is 1 order of magnitude larger than the topological regimes in semiconductor wires [13,34]. Finally, we performed a time-dependent calculation to show the non-Abelian braiding dynamics of Majorana modes in a cross-shaped QAH junction. Such QAH structures can readily be extended to a scalable network and provide new platforms for topological quantum computation.
Model Hamiltonian. The effective Hamiltonian of QAH insulator can be written as [24,25]

$$
H_{QAH} = \sum_{\mathbf{k}} [\Psi_{\mathbf{k}}^\dagger \left( \bar{h} v_F k_x \sigma_x \tau_z - \bar{h} v_F k_y \sigma_y \tau_z + m(\mathbf{k}) \tau_z \right) + M_1 \sigma_x] \Psi_{\mathbf{k}}.
$$

(1)

Here, $\Psi_{\mathbf{k}} = [\psi_{\mathbf{k}1}, \psi_{\mathbf{k}1}^\dagger, \psi_{\mathbf{k}2}, \psi_{\mathbf{k}2}^\dagger]$ is a four-component electron operator with the momentum $\mathbf{k}$, where $t$ ($b$) denotes the top (bottom) layer of topological insulator surface and $\dagger$ ($\dagger$) denotes the spin index. The Pauli matrices $\sigma_{x,y,z}$ operate on spin space and $\tau_{x,z}$ operate on the layer index. Fermi velocity of the surface states is denoted by $v_F$ and $m(\mathbf{k}) = m_0 - m_1 (k_x^2 + k_y^2)$ describes the effective coupling between the top and bottom layers. $M_1$ denotes spin splitting in the $z$ direction due to the magnetic doping in topological insulator and external magnetic field. To be specific, we set $m_0 = -5$ meV and $m_1 = 15$ eV Å $^2$ [35]. When $M_z < -|m_0|$ and $M_z > |m_0|$, the system is in the QAH phase with Chern number $N = 1$ and $-1$ respectively. On the other hand, the system is a trivial insulator for $-|m_0| < M_z < |m_0|$. We have shown recently that this effective Hamiltonian can accurately describe the experimental data in the conductance measurements of QAH-superconductor heterostructures [36].

As described earlier, when the sample is narrowed down to a quasi-1D limit (when the width of the sample is comparable to the localization length of the chiral edge modes), as shown in Fig. 1(b), the two chiral edge states can couple to form a helical channel. In the calculations for Figs. 1(c) and 1(d), the localization length $\xi \approx \hbar v_F / E_x$ of two edge modes is about 100 nm with a bulk gap of $E_x = 3$ meV. When the width of QAH system is much larger than the localization length, for example, $L_y = 800$ nm $\gg \xi$, the two edge modes on the opposite sides are not coupled [see Fig. 1(c)]. However, when we reduce the width of the QAH system to be comparable to the localization length of 100 nm, the two edge modes are coupled and open up a sizable gap of about 5 meV [37]. The resulting energy spectrum is shown in Fig. 1(d). Due to the increased confinement, the bulk states are pushed to higher energy which leaves a well separated helical channel from the rest of the states. This important feature gives rise to a large topological superconducting regime ($\approx 10$ meV) in the quasi-1D QAH/SC heterostructure as discussed below.

Localized Majorana modes in QAH/SC heterostructures. In proximity to an $s$-wave superconductor, the quasi-1D QAH/SC heterostructure Hamiltonian can be expressed as [24]

$$
H_{BDHG} = \sum_{k_x, n_y} \sum_{n_z = 1}^{N_y} \Phi_{k_x, n_y}^\dagger \left( m(\mathbf{k}) \tau_z - \bar{h} v_F k_x \sigma_x \tau_z + M_1 \tau_z - \mu \right) \Phi_{k_x, n_y} + \Delta \sigma_y \tau_z \left( \frac{1}{2} \frac{\bar{h} v_F}{\Delta} \sigma_y \tau_z \Phi_{k_x, n_y}^\dagger \Phi_{k_x, n_y}^\dagger \right)
$$

(2)

where $\Phi_{k_x, n_y} = [\Psi_{k_x, n_y}, \Psi_{k_x, n_y}^\dagger]$, and $\Psi_{k_x, n_y}^\dagger$ creates an electron at the $n_y$ site with momentum $k_x$. $\Delta$ is the pairing potential on the top surface due to the superconductor and $\mu$ is the unit matrix. $\mu$ is the chemical potential. $m_1 = m_0 - m_1 (k_x^2 + k_y^2)$ is defined in real space with Kronecker delta $\delta_{ij}$; As a consequence, $H_{BDHG}$ satisfies a chiral symmetry $C H_{BDHG}(k_x) C^{-1} = -H_{BDHG}(k_x)$, and the system is in the BDI class with $T^2 = 1$ and $P^2 = 1$, where $C = PT = UT_s$. Therefore, the topological properties of the system is characterized by a topological invariant $\nu_{BDI}$ for BDI class Hamiltonians [38,39].

In Fig. 2(a), we show the number of bands $n$ of the quasi-1D QAH (without superconductor) cut by the Fermi energy $\mu$ with Zeeman field $M_z$. In the absence of Zeeman field $M_z = 0$, the system has time-reversal symmetry $T = \sigma_y$, giving rise to two folder Kramer’s degeneracies. The Fermi energy can only cut through an even number of bands $n = 0, 2, 4$. With increasing $M_z$, each one-dimensional degenerate band splits into two branches and there can be an odd number of bands at the Fermi energy. As shown in Fig. 2(b), the system is topological when there is an odd number of bands at the Fermi energy. Indeed, there is a $N_{BDI} = 2$ phase when two subbands are partially occupied. In this phase, there are two Majorana fermions at each end of the wire which are protected by the chiral symmetry. Unfortunately, disorder breaks this.
chiral symmetry and the two Majorana modes at one end of the wire will couple into a trivial fermionic mode. Therefore, only the $N_{BDI} = 1$ phase is topologically nontrivial in the presence of disorder as the single Majorana can be protected by the particle-hole symmetry alone. It is important to note that the $N_{BDI} = 1$ topological region is very wide, which can be tuned by chemical potential $\mu$ or Zeeman field $M_z$. For example, when $M_z > m_1 = 5$ meV, which can be easily reached by tuning the external magnetic field, the lowest band originating from the QAH edge mode is well separated from the second lowest band originating from the QAH bulk band. This gives rise to a topological regime of about 10 meV wide in terms of chemical potential as shown in Fig. 2(b). The topological regime is about ten times larger than that of semiconductor wire systems [13,34]. This regime is also much wider than the two-dimensional chiral topological regime which requires $\Delta$ to be larger than $M_z$ [20,22,24]. Here, there are no such requirements. Therefore, the quasi-1D QAH structure hosts a large topological regime which is readily accessible experimentally.

To detect the Majorana modes, one may attach a macroscopic lead to the QAH system as shown in Fig. 3(a). When the QAH system possesses chiral fermionic modes, an electron mode (black arrows) comes into the QAH and is reflected as a hole mode (blue arrows) by a Majorana mode $\gamma$ (red dot). The zero-bias conductance $G$ from the lead to the superconductor as a function of Zeeman field $M_z$ with chemical potential $\mu = 5$ meV. (b) The two terminal conductance vs electric voltage $eV$ for different $\mu$ with $M_z = 6$ meV and $\Delta = 1$ meV. Other parameters are the same as those in Fig. 2(b).

for quantum computation can be easily fabricated by standard techniques from two-dimensional QAH systems. In Fig. 4(a), the cross-shaped QAH is fabricated on the superconductor with four gates (G1–G4) on the top. Initially, G1 and G3 are turned on (potential barriers are created) while G2 and G4 are turned off (no gating potential is applied), and the QAH/SC are divided into three topological nontrivial parts such that

![Image](image-url)

**FIG. 2.** (a) The number $n$ denotes the number of bands of the quasi-1D QAH (without superconductivity) cut by the Fermi energy as a function of chemical potential $\mu$ and effective Zeeman field $M_z$. The width and parameters of the quasi-1D system are the same as in Fig. 1(d). (b) The topological invariant $N_{BDI}$ in the superconducting phase as a function of $\mu$ and $M_z$. The parameters are the same as (a) except that a pairing potential $\Delta = 1$ meV is introduced on the top surface.

![Image](image-url)

**FIG. 3.** (a) Schematic plot of two-terminal device for the detection of Majorana zero modes. A lead is attached to a QAH system while the narrow region of the QAH system is in proximity to an s-wave superconductor to create the Majorana zero energy mode. An electron mode from the edge state of the QAH system (black arrows) is reflected as a hole mode (blue arrows) by a Majorana mode $\gamma$ (red dot). (b) The projection of wave function $|\phi(t)\rangle$ onto the initial eigenstate $|n_1\rangle$ as a function of time, where $\phi(t) = \text{Tr}_c \int_0^T e^{i[H_c - \Delta]t} |n_1\rangle \langle n_2|$. The time-ordered operator $\mathcal{T}$ and $H_c$, is a realistic tight-binding model describing the cross-shaped QAH junction. The six-stage process of braiding $\gamma_1$ and $\gamma_6$ is described in the main text. The final states are orthogonal to the initial states after braiding and non-Abelian statistics is clearly demonstrated. The total braiding time for the six steps is $6T = 14.4 \text{ ns}$. Other parameters are the same as those in Fig. 3(c).

![Image](image-url)

**FIG. 4.** (a) Schematic plot of a cross-shaped QAH system in proximity to a superconductor with four tunable gates (G1–G4) on the top. Initially, when G1 and G3 are turned on with G2 and G4 are turned off, the system is divided into three topologically nontrivial parts with six Majorana modes ($\gamma_1$–$\gamma_6$). (b) The projection of wave function $|\phi(t)\rangle$ onto the initial eigenstate $|n_1\rangle$ as a function of time, where $\phi(t) = \text{Tr}_c \int_0^T e^{i[H_c - \Delta]t} |n_1\rangle \langle n_2|$. The time-ordered operator $\mathcal{T}$ and $H_c$, is a realistic tight-binding model describing the cross-shaped QAH junction. The six-stage process of braiding $\gamma_1$ and $\gamma_6$ is described in the main text. The final states are orthogonal to the initial states after braiding and non-Abelian statistics is clearly demonstrated. The total braiding time for the six steps is $6T = 14.4 \text{ ns}$.
there are six Majorana modes in the system \((\gamma_1-\gamma_6)\) as shown in Fig. 4(a).

The effective Hamiltonian of the QAH cross-shaped junction can be written as

\[ H_{\text{eff}} = i\epsilon_1 \gamma_1 \gamma_2 + i\epsilon_2 \gamma_3 \gamma_4, \]

where \(\epsilon_{1,2}\) are the coupling energies of Majorana modes. Here we ignore \(\gamma_2\) and \(\gamma_6\) in the Hamiltonian, since they are well separated. Now the system contains two fermionic modes \(c_1 = (\gamma_1 + i\gamma_2)/2\) and \(c_2 = (\gamma_1 + i\gamma_3)/2\), and the low-energy Hilbert space contains four qubit states \(|n_1n_2\rangle\) with particle number \(n_{1,2} = 0, 1\). The ground state is defined as \(c_1|00\rangle = c_2|00\rangle = 0\). The braiding operator \(B|\gamma_1\gamma_2\rangle = \exp(\frac{i\pi}{2}|\gamma_1\gamma_2\rangle)\) transforms the Majorana modes as \(|\gamma_1\rangle \rightarrow |\gamma_2\rangle\) and \(|\gamma_3\rangle \rightarrow -|\gamma_2\rangle\) [43]. Exchanging \(\gamma_2\) and \(\gamma_3\) twice would lead to a sign change \(|\gamma_1\rangle \rightarrow -|\gamma_2\rangle\) and \(|\gamma_3\rangle \rightarrow -|\gamma_3\rangle\), and then \(c_1 = (\gamma_1 + i\gamma_3)/2 \rightarrow c_1\) and \(c_2 = (\gamma_1 + i\gamma_2)/2 \rightarrow c_2\). As a result, if the initial state of the system is \(|00\rangle\), the final state \(|11\rangle \rightarrow B^3|\gamma_2\gamma_3\rangle|00\rangle\) becomes orthogonal to the initial state after exchanging \(\gamma_2\) and \(\gamma_3\) twice.

In the time-dependent simulations using a realistic Hamiltonian, \(\gamma_2\) and \(\gamma_3\) can be exchanged by taking three steps: first, move \(\gamma_2\) upward by turning off G1 and then turning on G2; second, move \(\gamma_1\) to the left by turning off G3 and then turning on G1; finally, move \(\gamma_2\) to the right by turning off G2 and then turning on G3. Exchanging \(\gamma_2\) and \(\gamma_3\) twice yields a full braiding process. In Fig. 4(b), when the initial state is set to \(|00\rangle\) (blue line), we reach the final state \(|11\rangle\) (red line) after braiding \(\gamma_2\) and \(\gamma_3\) in the six-step gating process as described above. Indeed, the final state \(|11\rangle\) is orthogonal to the initial state \(|00\rangle\) after the braiding process. This clearly justifies the non-Abelian nature of the Majorana braiding process and thus QAH/SC heterostructures can provide new platforms for the non-Abelian nature of the Majorana braiding process and QAH/SC heterostructures [21,22,24]. Therefore, the results discussed in this work do not depend on the origin of the half-quantized plateaus observed recently by He et al. [21] which is under intense debate [36,45-47].

In the 2D case, superconducting pairing is induced to the bulk states. As a result, the superconducting pairing must be larger than the bulk gap to drive a topological phase transition. In our current proposal, we make use of the chiral edge states are gapless and they can form a helical channel. When superconducting pairing is induced on this helical channel (and no matter how small the induced pairing gap is), a topological superconductor is formed. This is the reason why the topological regime in our quasi-1D proposal is much wider than that in the 2D case. This is a very important advantage of the current proposal.

Moreover, QAH systems are very different from ferromagnetic metal or semiconductors. In ferromagnetic systems or semiconductors, due to the high chemical potential, many subbands are created at Fermi energy when the systems are narrowed down to the quasi-1D limit. For QAH systems, no extra subbands are created when the samples are narrowed down to the quasi-1D limit as the bulk is gapped. This is another important advantage of the current proposal. For experimental realization, it is crucial that the width of the quasi-1D QAH sample is comparable or smaller than the coherence length of the parent superconductor so that superconducting pairing can be induced on the chiral edge states effectively.

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1. A. Kitaev, Ann. Phys. (NY) 303, 2 (2003).
2. C. Nayak, S. H. Simon, A. Stern, M. Freedman, and S. D. Sarma, Rev. Mod. Phys. 80, 1083 (2008).
3. N. Read and D. Green, Phys. Rev. B 61, 10267 (2000).
4. V. Gurarie, L. Radzihovsky, and A. V. Andreev, Phys. Rev. Lett. 94, 230403 (2005).
5. M. Stone and S. B. Chung, Phys. Rev. B 73, 014505 (2006).
6. A. Y. Kitaev, Phys. Usp. 44, 131 (2001).
7. L. Fu and C. L. Kane, Phys. Rev. Lett. 100, 096407 (2008).
8. H.-H. Sun, K.-W. Zhang, L.-H. Hu, C. Li, G.-Y. Wang, H.-Y. Ma, Z.-A. Xu, C.-L. Gao, D.-D. Guan, Y.-Y. Li, C. Liu, D. Qian, Y. Zhou, L. Fu, S.-C. Li, F.-C. Zhang, and J.-F. Jia, Phys. Rev. Lett. 116, 257003 (2016).
9. J. J. He, T. K. Ng, P. A. Lee, and K. T. Law, Phys. Rev. Lett. 112, 037001 (2014).
10. R. M. Lutchyn, J. D. Sau, and S. D. Sarma, Phys. Rev. Lett. 105, 077001 (2010).
11. J. Alicea, Phys. Rev. B 81, 125318 (2010).
12. Y. Oreg, G. Refael, and F. von Oppen, Phys. Rev. Lett. 105, 177002 (2010).
13. V. Mourik, K. Zuo, S. M. Frolov, S. R. Plissard, E. P. A. M. Bakkers, and L. P. Kouwenhoven, Science 336, 1003 (2012).
14. A. Das, Y. Ronen, Y. Most, Y. Oreg, M. Heiblum, and H. Shtrikman, Nat. Phys. 8, 887 (2012).
15. M. T. Deng, C. L. Yu, G. Y. Huang, M. Larsson, P. Caroff, and H. Q. Xu, Nano Lett. 12, 6414 (2012).
[16] K. T. Law, P. A. Lee, and T. K. Ng, Phys. Rev. Lett. 103, 237001 (2009).

[17] M. Wimmer, A. R. Akhmerov, J. P. Dahlhaus, and C. W. J. Beenakker, New J. Phys. 13, 053016 (2011).

[18] F. Nichele, A. C. C. Drachmann, A. M. Whiticar, E. C. T. O’Farrell, H. J. Suominen, A. Fornieri, T. Wang, M. C. Gardner, C. Thomas, A. T. Hatke, P. Krogsrup, M. J. Manfra, K. Flensberg, and C. M. Marcus, Phys. Rev. Lett. 119, 136803 (2017).

[19] H. Zhang et al., arXiv:1710.10701.

[20] T. Karzig, C. Knapp, R. M. Lutchyn, P. Bonderson, M. B. Hastings, C. Nayak, J. Alicea, K. Flensberg, S. Plugge, Y. Oreg, C. M. Marcus, and M. H. Freedman, Phys. Rev. B 95, 235305 (2017).

[21] Q. L. He, L. Pan, A. L. Stern, E. Burks, X. Che, G. Yin, J. Wang, B. Lian, Q. Zhou, E. S. Choi, K. Murata, X. Kou, T. Nie, Q. Shao, Y. Fan, S.-C. Zhang, K. Liu, J. Xia, and K. L. Wang, Science 357, 294 (2017).

[22] X. L. Qi, T. L. Hughes, and S. C. Zhang, Phys. Rev. B 82, 184516 (2010).

[23] S. B. Chung, X. L. Qi, J. Maciejko, and S. C. Zhang, Phys. Rev. B 83, 100512(R) (2011).

[24] J. Wang, Q. Zhou, B. Lian, and S. C. Zhang, Phys. Rev. B 92, 064520 (2015).

[25] R. Yu, W. Zhang, H. J. Zhang, S. C. Zhang, X. Dai, and Z. Fang, Science 329, 61 (2010).

[26] C.-Z. Chang, J. Zhang, X. Feng, J. Shen, Z. Zhang, M. Guo, K. Li, Y. Ou, P. Wei, L.-L. Wang, Z.-Q. Ji, Y. Feng, S. Ji, X. Chen, J. Jia, X. Dai, Z. Fang, S.-C. Zhang, K. He, Y. Wang, L. Lu, X.-C. Ma, and Q.-K. Xue, Science 340, 167 (2013).

[27] J. G. Checkelsky, R. Yoshimi, A. Tsukazaki, K. S. Takahashi, Y. Kozuka, J. Fafson, M. Kawasaki, and Y. Tokura, Nat. Phys. 10, 731 (2014).

[28] X. Kou, S.-T. Guo, Y. Fan, L. Pan, M. Lang, Y. Jiang, Q. Shao, T. Nie, K. Murata, J. Tang, Y. Wang, L. He, T.-K. Lee, W.-L. Lee, and K. L. Wang, Phys. Rev. Lett. 113, 137201 (2014).

[29] A. J. Bestwick, E. J. Fox, X. Kou, L. Pan, K. L. Wang, and D. Goldhaber-Gordon, Phys. Rev. Lett. 114, 187201 (2015).

[30] Y. Feng, X. Feng, Y. Ou, J. Wang, C. Liu, L. Zhang, D. Zhao, G. Jiang, S. C. Zhang, K. He, X. Ma, Q. K. Xue, and Y. Wang, Phys. Rev. Lett. 115, 126801 (2015).

[31] C.-Z. Chang, W. Zhao, D. Y. Kim, H. Zhang, B. A. Assaf, D. Heiman, S.-C. Zhang, C. Liu, M. H. W. Chan, and J. S. Moodera, Nat. Mater. 14, 473 (2015).

[32] A. Kandala, A. Richardella, S. Kemperling, C.-X. Liu, and N. Samarth, Nat. Commun. 6, 7434 (2015).

[33] D. Litinski, M. S. Kesselring, J. Eisert, and F. von Oppen, Phys. Rev. X 7, 031048 (2017).

[34] J. Liu, A. C. Potter, K. T. Law, and P. A. Lee, Phys. Rev. Lett. 109, 267002 (2012).

[35] Y. Zhang, K. He, C.-Z. Chang, C.-L. Song, L.-L. Wang, X. Chen, J.-F. Jia, Z. Fang, X. Dai, W.-Y. Shan, S.-Q. Shen, Q. Niu, X.-L. Qi, S.-C. Zhang, X.-C. Ma, and Q.-K. Xue, Nat. Phys. 6, 584 (2010).

[36] C.-Z. Chen, J. J. He, D.-H. Xu, and K. T. Law, Phys. Rev. B 96, 041118 (2017).

[37] J. Klinovaja and D. Loss, Phys. Rev. B 92, 121410(R) (2015).

[38] A. P. Schnyder, S. Ryu, A. Furusaki, and A. W. W. Ludwig, Phys. Rev. B 78, 195125 (2008).

[39] S. Tewari and J. D. Sau, Phys. Rev. Lett. 109, 150408 (2012).

[40] P. A. Lee and D. S. Fisher, Phys. Rev. Lett. 47, 882 (1981).

[41] C. S. Amorim, K. Ebihara, A. Yamakage, Y. Tanaka, and M. Sato, Phys. Rev. B 91, 174305 (2015).

[42] J. Alicea, Y. Oreg, G. Refael, F. von Oppen, and M. P. A. Fisher, Nat. Phys. 7, 412 (2011).

[43] D. A. Ivanov, Phys. Rev. Lett. 86, 268 (2001).

[44] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevB.97.104504 for further information about details of time-dependent simulations of braiding Majorana modes.

[45] W. Ji and X.-G. Wen, arXiv:1708.06214.

[46] Y. Huang, F. Setiawan, and J. D. Sau, arXiv:1708.06752.

[47] B. Lian, J. Wang, X.-Q. Sun, A. Vaezi, and S.-C. Zhang, arXiv:1709.05558.