Forecasting stock index based on hybrid artificial neural network models

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ABSTRACT
Forecasting stock index is a crucial financial problem which is recently received a lot of interests in the field of artificial intelligence. In this paper we are going to study some hybrid artificial neural network models. As main result, we show that hybrid models offer us effective tools to forecast stock index accurately. Within this study, we have analyzed the performance of classical models such as Autoregressive Integrated Moving Average (ARIMA), Artificial Neural Network (ANN) model and the Hybrid model, in connection with real data coming from Vietnam Index (VNINDEX). Based on some previous foreign data sets, for most of the complex time series, the novel hybrid models have a good performance comparing to individual models like ARIMA and ANN. Specifically, our results tell that the Hybrid combination model delivers smaller Root Mean Square Error (RMSE) and Mean Absolute Error (MAE) than ARIMA and ANN models. The fitting curves demonstrate that the Hybrid model produces closer trend so better describing the actual data. Via our study with Vietnam Index, it is confirmed that the characteristics of ARIMA model are more suitable for linear time series while ANN model is good to work with nonlinear time series. The Hybrid model takes into account both of these features, so it could be employed in case of more generalized time series. As the financial market is increasingly complex, the time series corresponding to stock indexes naturally consist of linear and non-linear components. Because of these characteristic, the Hybrid ARIMA model with ANN produces better prediction and estimation than other traditional models. Key words: stock index, Hybrid models, Vietnamese stock market, ARIMA model, ANN model.

INTRODUCTION
In the past two decades, the most popular techniques used in forecasting stock prices are the statistical models and the artificial intelligence models (AI). Some most commonly used methods in the statistical models for time series analysis include, e.g., Autoregressive Integrated Moving Average (ARIMA) or the well-known Box-Jenkins model, Exponential Smoothing model (ESM), and Generalized Autoregressive Conditional Heteroskedasticity (GARCH) volatility. Due to the fact that the mean and variance of financial time series change overtime, and, hence, the series are not linear. More precisely, financial time series often contain both linear and non-linear patterns. Therefore, one of the main restrictions in these traditional models is that they only contain a linear structure. In fact, Refenes et al.¹ showed that the traditional statistical models, such as ARIMA model, for forecasting have main limitations in applications to non-linear data set such as stock indices, exchange rates. The recent development in the theory of computational intelligence provides powerful mathematical tools for private investors, portfolio managers and also bankers to exploit the big data, especially, big data in finance. The AI models and machine learning techniques, e.g., the Artificial Neural Network models (ANN) are introduced and utilized to overcome these restrictions. These models contain two components that are linear and non-linear parts. Recently, a new approach which combines ARIMA and ANN models for financial time series has been studied, e.g., in Zhang², Wang et al.³. This combination is called the hybrid model. It is showed that the hybrid model gives more accurate result for forecasting time series, especially, for stock prices. The basic idea of hybrid ARIMA and Artificial Neural Network model is that the non-linear patterns can be presented as the residuals of the linear ARIMA model which can be modeled by using artificial neural networks. Furthermore, the relationship between the linear and non-linear components is assumed to be additive. In this study we utilize the hybrid model to forecast VNINDEX stock price. We find out the suitable ARIMA and ANN models for the time series and then find out the appropriate a hybrid model which combines the ARIMA and ANN models.
more, we compare the results between hybrid model and the individual ARIMA and ANN models in terms of forecasting accuracy based on performance criteria such as Root Mean Square Error (RMSE), Normalized Mean Square Error (NMSE) and Mean Absolute Error (MAE).

**FORECASTING METHODOLOGY**

In this section we give a brief description on ARIMA and Artificial Neural Network models. Furthermore, we demonstrate the basic principle in the hybrid model from ARIMA and ANN models.

**The ARIMA model**

ARIMA model was first initiated by Box and Jenkins. This model is one of the most general class of models for forecasting a time series which can be made to be stationary by differencing. More precisely, ARIMA model is generalized from ARMA model (autoregressive moving average) in which the assumption on stationarity of time series is not necessary. The important characterization of ARIMA model is that the predictions of the behaviour of a time series in the future depend on the past observations by a linear function and random errors, i.e., the ARIMA equation for forecasting a stationary series \( Y_t \) has the following form

\[
Y_t = \phi_0 + \phi_1 Y_{t-1} + \phi_2 Y_{t-2} + \cdots + \phi_p Y_{t-p} + \epsilon_t - \theta_1 \epsilon_{t-1} - \theta_2 \epsilon_{t-2} - \cdots - \theta_q \epsilon_{t-q},
\]

where \( \epsilon_t \sim N(0, \sigma^2) \) is the random error. The parameter \( p \) is the number of autoregressive terms and \( q \) is the number of lagged forecast errors in the prediction equation.

It is seen that ARIMA processes have two components which are Autoregressive model (AR) of order \( p \) and Moving-Average (MA) model.

**The artificial neural network approach**

One of the most important advantages of an Artificial Neural Networks is to approximate various complex non-linear time series. The ANN is developed from statistical learning algorithm based on mimicking the neural networks in the human brain. It can process parallelly from information from data, and, hence, the ANN provides a powerful tool for forecasting time series more accurately. The ANN model consists of layers which are an input layer, output layer and single or more hidden layers. However, a single layer is the most common in modelling and forecasting for time series (see, e.g.,\(^5\)). The algorithm of the ANN can be described as follows. The input layer has one or more inputs where an input is a vector value. Each node in an input layer can be connected to the nodes of the first hidden layer. The data go to the network through hidden layers until attaining the output layer, for example, see the following Figure 1.

Intuitively Speaking, let \( Y_t \) be a time series. The relationship between the future value (the output) and its past values (the inputs) \( Y_{t-1}, Y_{t-2}, \ldots, Y_{t-p} \) can be represented by the following equation

\[
Y_t = a_0 + \sum_{j=1}^{q} a_j f \left( \omega_{0j} + \sum_{i=1}^{p} \omega_{ij} Y_{t-i} \right) + \epsilon_t, \tag{1}
\]

Where, \( a_t \) and \( \omega_{ij}, i = 1, 2, \ldots, p; j = 1, 2, \ldots, q \) are parameters of the model. They are called the connection weight between layers of the model. Parameters \( p \) and \( q \) are the number of input nodes and the number of hidden nodes in the model. The function \( f \) is the transfer function of the hidden layer taking the form

\[
f(x) = \frac{1}{1 + e^{-x}}
\]

It is seen that \( f \) is the logistic function\(^6\) or the sigmoid function taking values on \([0, 1]\). Furthermore, \( f \) is real-valued and differentiable and has some properties such as non-positive first derivative with one local minimum and one local maximum. From (1), we see that the ANN model forecasts the future value by performing a non-linear functional mapping of the past observations. Therefore, we can formulate its general mathematical equation as follows

\[
Y_t = \phi \left( Y_{t-1}, Y_{t-2}, \ldots, Y_{t-p}, \omega \right) + \epsilon_t,
\]

Where, \( \omega \) is the vector of parameter and the function \( \phi \) is determined by the network structure and appropriate weights. Therefore, ANN can be seen as a non-linear autoregressive model.

The main task when dealing with ANN model for a time series is to select a correct the lagged observations \( p \) and an appropriate number of hidden nodes \( q \). Unfortunately, there is no theoretical methods to guide the selection of these parameters, and, hence, in practice, selecting the appropriate values \( p \) and \( q \) is often conducted from experiments.
The hybrid approach

As far as we know that ARIMA model is a good performance for forecasting linear time series and ANN model is better selection for forecasting non-linear time series. However, both models are not good enough for fitting a more complex time series. Since, a complex time series can be decomposed into a linear component and a non-linear component, e.g., Fourier decomposition. Hence, the hybrid model is employed to model this type of time series in which ARIMA and ANN approaches can be deployed to model the linear component and the non-linear component, respectively (see, 2,3,7). More precisely, a time series $X_t$ can be represented as

$$X_t = L_t + N_t,$$

where $L_t, N_t$ denote the linear, non-linear components, respectively. These components can be fitted from data. First stage, ARIMA approach is used to model the linear component and, then, the residuals et from the linear model can be seen as the non-linear relationship. Hence, we can apply the ANN approach to this component. Denote $\hat{L}_t$ the forecast value at time $t$, we have

$$e_t = X_t - \hat{L}_t.$$  \hspace{1cm} (3)

By ANN approach, $e_t$ takes the form

$$e_t = \varphi (e_{t-1}, e_{t-2}, \ldots, e_{t-p}, \omega) + \epsilon_t,$$  \hspace{1cm} (4)

where, $\varphi$ is a non-linear function determined by the neural network and $\epsilon_t$ is the random error. Denote $\hat{N}_t$ the forecast value from (4). From (2), (3) and (4) we have the forecast value $\hat{X}_t$ of the series

$$\hat{X}_t = \hat{L}_t + \hat{N}_t.$$  \hspace{1cm} (5)

So, there are two steps to perform the hybrid ARIMA neural network model as follows

(i) forecast values $\hat{L}_t$ (resulted from ARIMA model)
(ii) forecast residuals $\hat{N}_t$ (resulted from ARIMA model) by ANN model

DATA - RESULTS

Data set

In this study the weekly closing prices for VNINDEX from January 4, 2006 to September 28, 2018 are used (Figures 2 and 3). There are total 663 trading weeks in this period. The data is divided into two periods, the first period includes 654 weeks (as a training set) that are used for model estimation and the second period includes 9 weeks (as a test set) that is reserved for forecasting and evaluation.

Financial time series are often not stationary, especially stock prices. Transform stock prices into log return prices is the most common method in analysing financial data. Let $P_t$ be the stock price at time $t$. The log returns $R_t$ are defined as

$$R_t := \log \left( \frac{P_t}{P_{t-1}} \right).$$

More details, we refer to 8 for good properties of log return. The log returns are also called continuously compounded returns. The plots of stock prices and weekly log returns are shown in the following Figure 2 and Figure 3.

Error measures

We introduce some of the most common error measures or accuracy measures widely used for comparing different forecasts in financial time series. These measures are used to identify which methods is one of the most suitable forecast methods. The most preferred measure used for forecasting accuracy of a model is the Root Mean Square Error (RMSE), see, e.g., R. Carbone and J. S. Armstrong 9 for more details. It is defined as

$$RMSE := \sqrt{\frac{\sum (Y_t - \hat{Y}_t)^2}{N}},$$

where $N$ is the sample size.
The following Mean Absolute Percentage Error (MAPE) is also used as a common error measure (see\textsuperscript{10})

\[ MAPE := \frac{1}{N} \sum \left| \frac{Y_i - \hat{Y}_i}{Y_i} \right|. \]

Another most popular error measure is known as the Mean Absolute Error (MAE):

\[ MAE := \frac{1}{N} \sum |Y_i - \hat{Y}_i|. \]

It is seen that, this measure is easy to both understand and compute.

**Results for price data**

We use ARIMA, ANN and Hybrid model to fit VNINDEX data. We compare these models and chose the best model for this data set. There are a number studies fitting financial data by using these models and show that the hybrid model is the best model for fitting and forecasting closing prices of market (see\textsuperscript{2,3,11,12}). In case Vietnamese market, we also see that the hybrid is the best model for fitting VNINDEX, see the following table for comparing error measures of these models.

The comparison between the actual values and fitted values of ARIMA and Hybrid models are given in Figure 4. This figure shows that Hybrid model has a good performance in fitting VNINDEX.

**DISCUSSIONS**

This work is one first attempt applying sophisticated quantitative models to study VNINDEX. To strengthen our results, further data sets and models should be used for testing and validation. We are going to investigate other stock indexes given in Thomson Reuters database as well as explore potential developed models and their necessary improvement. We also interested in studying whether different indexes coming from different countries favor the same type of models, or create country-associated effect.

**CONCLUSIONS**

In this study, we have analyzed the performance classical ARIMA, ANN model and the Hybrid model for describing VNINDEX. Generally, for almost complex time series, the novel hybrid models have a better performance than individual models ARIMA and ANN. For Vietnamese stock market, the results show that the Hybrid model also gives much better forecasting accuracy as compared with ARIMA and ANN models.

**ABBREVIATIONS**

AI: Artificial Intelligence
ARIMA: Autoregressive Integrated Moving Average
ESM: Exponential Smoothing Model
Table 1: Error Measures

|       | MAE      | RMSE       |
|-------|----------|------------|
| ARIMA | 0.006225405 | 6.597903e-05 |
| Hybrid | 0.005496027  | 5.426601e-05 |
| ANN   | 0.005751329  | 5.562526e-05 |

**Figure 4**: Fitting with ARIMA and Hybrid models.

**GARCH**: Generalized Autoregressive Conditional Heteroskedasticity

**ANN**: Artificial Neural Network model

**RMSE**: Root Mean Square Error

**NMSE**: Normalized Mean Square Error

**MAE**: Mean Absolute Error

**VNINDEX**: Vietnam Index, a capitalization-weighted index of all the companies listed on the Ho Chi Minh City Stock Exchange

**COMPETING INTERESTS**
The authors declare that they have no conflict of interest.

**AUTHORS’ CONTRIBUTIONS**
Ta Quoc Bao and Le Thi Thanh An initiate the idea, study relevant models and seek for the data. Ta Quoc Bao and Le Nhat Tan build the main programs for numerical simulations. All authors check the simulation and contribute for the interpretation of the results. Ta Quoc Bao and Le Thi Thanh An edit and revise the text. All authors check and approve the article.

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Dự báo chỉ số cổ phiếu bằng các mô hình mạng kinh nhân tạo kết hợp

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Tóm tắt
Dự báo chỉ số cổ phiếu là một trong những vấn đề tài chính quan trọng và gắn đầy đủ thu hút được nhiều sự quan tâm từ các chuyên gia trong lĩnh vực thống kê và chính sách kinh tế. Trong nghiên cứu này, chúng tôi sử dụng một số mô hình mạng kinh nhân tạo để dự báo chính xác hơn chỉ số chứng khoán. Kết quả chính cho thấy mô hình kết hợp giữa các mô hình mạng kinh nhân tạo Hybrid ARIMA và ANN và mô hình kinh nhân tạo kết hợp Hybrid ARIMA và ANN. Dựa trên các số liệu từ các nước, đối với hầu hết các chuỗi thời gian phức tạp, mô hình kết hợp mới cho khả năng dự báo tốt hơn so với các mô hình riêng lẻ ARIMA và ANN. Đối với thị trường cổ phiếu Việt Nam, kết quả cũng cho thấy các mô hình kết hợp mới dự báo chính xác hơn so với các mô hình ARIMA và ANN. Các kết quả của nghiên cứu cho thấy mô hình kết hợp Hybrid cho sai số nhỏ hơn so với hai mô hình đơn ARIMA và ANN. Các đô thị xấp xỉ chỉ ra rằng mô hình Hybrid phản ánh chính xác xu hướng tăng giảm và gần với dữ liệu thực tế hơn. Đặc điểm của mô hình ARIMA thường thích hợp cho các chuỗi thời gian tuyến tính trong khi mô hình ANN hay được sử dụng để dự báo cho các chuỗi thời gian phi tuyến. Mô hình Hybrid kết hợp được cải thiện tốt trên các mô hình đơn cho các chuỗi thời gian phức tạp. Do thị trường tài chính ngày càng phức tạp nên đặc điểm của mô hình kết hợp Hybrid ARIMA và ANN có thể dự báo và ước lượng tốt hơn các mô hình truyền thống khác.

Từ khóa: Chỉ số cổ phiếu, mô hình kết hợp, thị trường cổ phiếu Việt Nam, mô hình ARIMA, ANN

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