Flux pinning in (1111) iron-pnictide superconducting crystals

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Local magnetic measurements are used to quantitatively characterize heterogeneity and flux line pinning in PrFeAsO 1−y and NdFeAs(O,F) superconducting single crystals. In spite of spatial fluctuations of the critical current density on the mesoscopic scale, it is shown that the major contribution comes from collective pinning of vortex lines by microscopic defects by the mean-free path fluctuation mechanism. The defect density extracted from experiment corresponds to the dopant atom density, which means that dopant atoms play an important role both in vortex pinning and in quasiparticle scattering. In the studied underdoped PrFeAsO 1−y and NdFeAs(O,F) crystals, there is a background of strong pinning, which we attribute to spatial variations of the dopant atom density on the scale of a few dozen to one hundred nm. These variations do not go beyond 5% – we therefore do not find any evidence for coexistence of the superconducting and the antiferromagnetic phase. The critical current density in sub-T fields is characterized by the presence of a peak effect, the location of which in the (B,T) plane is consistent with an order-disorder transition of the vortex lattice.

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I. INTRODUCTION

The characterization of the physical properties of new superconducting materials such as the recently discovered iron-pnictide superconductors 1–7 requires a good knowledge of sample morphology and microstructure. The measurement and interpretation of thermodynamic quantities such as the magnetization, the magnetic torque, 10 or the specific heat, or transport properties such as the resistance or irreversible magnetization, may be complicated by material inhomogeneity on microscopic or macroscopic length scales. On the other hand, microscopic disorder is well-known to be beneficial for vortex line pinning and high critical currents. Finally, from the defect-vortex interaction, one might hope to extract information on electronic scattering mechanisms in the iron-pnictide superconductors, as well as on the premise of phase coexistence. In underdoped pnictides especially, it has been argued that the coexistence of the low-doping anti-ferromagnetic state and the superconducting state at higher doping levels may affect physical properties. 9

Vortex pinning and the critical current density in the iron pnictide superconductors has mainly focussed on the so-called “122” compounds, since large single crystals of these are available. Most notably, magnetic flux penetration in Ba(Fe0.93Co0.07)2As2 has been studied using magneto-optical imaging by Prozorov et al. 11,12 The same authors reported on the irreversible magnetization and flux creep in this compound, and found qualitative agreement with collective creep in the so-called bundle regime. 13 The non-monotonous behavior of the sustainable current as function of magnetic field was interpreted in terms of a crossover to plastic creep. 14 A similar behavior was found for crystals with different doping levels; 12,14 the overall behavior of the critical current density as function of doping was attributed to the changing density of structural domain walls, that act as strong pinning centers. 15 Yamamoto et al. obtained similar results on the same Ba(Fe0.9Co0.1)2As2, but attributed the temperature- and field-dependent features of the critical current density to an inhomogeneous distribution of Co atoms. 16 Very large critical currents, as well as a non-monotonous width of the irreversible magnetization loops corresponding to a peak-effect in the critical current 17–21 were measured by Yang et al. in single crystalline Ba0.9K0.1Fe2As2, 22 who concluded to the presence of small-sized normal state regions in their samples. Finally, irreversible magnetization and flux creep measurements were conducted on SmFeAsO0.9F0.1 23 and polycrystalline NdFeAsO0.82F0.18,24,25 members of the “1111” family of compounds. In all the above cases, the critical current at low fields was characterized by a peak and negligible magnetic relaxation, followed by more pronounced thermally activated flux motion at higher fields,
which was found to be in qualitative agreement with the collective creep theory. However, no quantitative analysis of the data has been performed, and no definite consensus as to the defects at the origin of flux pinning has been established.

The aim of the present paper is the identification of defects responsible for flux pinning in single crystals of the (Re)FeAsO “1111” family of superconducting compounds. The microstructure is characterized by the undulation of the FeAs layers and the presence of sparse nanometer-sized defects, both of which do not seem to influence flux pinning. The largest contribution to the critical current \( j_c \) is shown to arise from the dopant atoms, which act as scatterers for quasi-particles in the vortex cores. One therefore deals with pinning by local variations of the mean-free path (\( \delta k \) mechanism). The temperature- and field dependence of \( j_c \) is very well described by collective flux pinning in the single-vortex limit, but superposed on a strong pinning contribution arising from small fluctuations of the doping level on the scale of dozens of nm.

II. EXPERIMENTAL DETAILS

PrFeAsO\(_{1-y}\) crystals (with the P4/mmm structure) were grown at 1300°C and 2 GPa from pressed pellets consisting of the starting materials PrAs, Fe, and Fe\(_2\)O\(_3\), in the nominal composition PrFeAsO\(_{0.6}\).\(^{26,27}\) The typical size of the crystals is 100 \( \times \) 100 \( \times \) 30 \( \mu m^3\); the average final composition corresponds to \( y \sim 0.1 \). A number of monolithic crystals from this batch has been previously used for the measurement of the superfluid density,\(^{28}\) the field of first flux penetration,\(^{27}\) and the electrical resistivity in the vicinity of the superfluid density,\(^{27}\) The low-field penetration depth \( \lambda_{ab}(T) \) (for currents parallel to the \( ab \) plane) is well described by a simple two-gap model, without any nodes of the order parameter. The magnitude of the low temperature penetration depth is \( \lambda_{ab}(0) = 280 \text{ nm} \).\(^{27}\) Table I gathers the superconducting properties of the compound, for which we establish a consensus as to the defects at the origin of flux pinning.

Several PrFeAsO\(_{1-y}\) crystals were prepared for Transmission Electron Microscopy (TEM). In each case, two crystals, of lateral dimensions \( \sim 100 \mu m \), were glued between 0.5 mm thick Si platelets; these were then thinned down until the crystals were flush with the edges. Further thinning yielded sections parallel to the \( c \)-axis, suitable for TEM. Figure 1a, a high resolution image of one of the sections, reveals the undulation of the FeAs layers. Figure 1c shows contrast associated with the presence of a linear dislocation core, occasional examples of which were found.

Three PrFeAsO\(_{1-y}\) crystals (\( \neq 1, 3, \) and 7) were characterized by X-ray diffraction using 28.3 keV (0.43811 Å) radiation on the CRISTAL beam at the SOLEIL synchrotron. Images of diffraction spots were collected on a 2D CCD detector when the sample was rotated around an axis in the \( ab \) plane. From the 360 measured images, successively collected during 1 s after a progression of 1° of the crystal rotation, layers of reciprocal space were numerically reconstructed. Three such sections, contain-
FIG. 2: (color online) Cuts through reciprocal space of the PrFeAsO$_{1−y}$ compound, reconstructed from synchrotron radiation X-ray diffraction on crystal # 7 (the same crystal as in Ref.27). (a) the [hk0] plane (b) the [0kl] plane; (c) the [h0l] plane.

The [hk0] section reveals very good translational order in the basal plane. However, the fulfilment of the Laue condition over extended streaks in the [h0l] and [0kl] planes shows that crystalline order along the c-axis is not as good. The pronounced elongation of both low- and higher order nodes in the [00l] direction indicates that this disorder more than likely originates from the undulation of the planes observed in TEM. Other kinds of c-axis disorder such as stacking faults or anti-phase boundaries would have yielded a larger broadening of nodes outside the [hk0] plane, as compared to the lower order nodes. From the elongation of the nodes at [100] and [010], we estimate the buckling of the layers to result in a variation of their orientation of up to 5°. The same results were obtained for all studied crystals.

The NdFeAsO$_9$F$_{0.1}$ crystals used in this study are the same as that of Ref. 29; they were synthesized at high pressure in a cubic, multi-anvil apparatus. The crystals, extracted from a polycrystalline batch, had dimensions $210 \times 320 \times 30$ μm$^3$ (# 1) and $150 \times 200 \times 50$ μm$^3$ (# 2), and critical temperatures $T_c = 34.5 \pm 1.5$ K (# 1) and $37.5 \pm 1$ K (# 2). The superconducting parameters of NdFeAs(O,F) of this particular doping level have been studied in Refs. 29 and 30, and are summarized in Table I.

In order to obtain the value and local distribution of $T_c$ and $j_c$, flux penetration into the superconducting crystals was imaged using the direct magneto-optical imaging (MOI) method. Crystalline inhomogeneity in the vicinity of the critical temperature was characterized using the Differential Magneto-Optical (DMO) method. In MOI, a ferrimagnetic garnet indicator with in-plane anisotropy is placed on top of the sample under study, and observed using a polarized light microscope. The presence of a non-zero perpendicular component $B_\perp$ of the magnetic induction is revealed, by virtue of the Faraday effect of the garnet, as a non-zero intensity of reflected light when the polarizers of the microscope are (nearly) crossed. Thus, light areas in the MO images correspond to areas of high perpendicular induction, while dark regions have small or zero $B_\perp$. In DMO, magneto-optical images taken at applied fields $H_a$ and $H_a + \Delta H_a$ (with $\Delta H_a = 1$ Oe) are subtracted; the procedure is repeated 100 times, and the subtracted images averaged.

The local critical current density of the investigated crystals was obtained by calibrating the luminous intensity of the MOI images, so as to obtain a map of the local induction. $j_c$ was then determined as twice the gradient of the local flux density, measured over an interval of length 20 μm perpendicular to the sample boundary, and averaged over a width of 20 μm (parallel to the sample boundary).

| compound            | $\lambda_0(0)$ | $\varepsilon(0)$ | $\xi_0(0)$ | $\varepsilon(0)$ | $j_0(0)$ | $G_I$ |
|---------------------|----------------|-----------------|------------|-----------------|----------|-------|
| PrFeAsO$_{0.9}$F$_{0.1}$ | 280 nm         | 0.4             | 1.8 nm     | $3.2 \times 10^{-12}$ Jm$^{-1}$ | $2 \times 10^{14}$ Am$^{-2}$ | $3 \times 10^{-3}$ |
| NdFeAsO$_{0.7}$F$_{0.1}$ | $270 \pm 40$ nm | 0.25            | 2.4 nm     | $3.5 \times 10^{-12}$ Jm$^{-1}$ | $1.6 \times 10^{12}$ Am$^{-2}$ | $3 \times 10^{-3}$ |

TABLE 1: Superconducting properties of the crystals used in this study.
III. RESULTS

A. PrFeAsO$_{1-y}$

Spatial inhomogeneity of the critical temperature in single crystals was investigated by the DMO images near the transition. A typical example is shown in Fig. 3a, depicting four DMO images, acquired with a $\Delta H_a = 1$ Oe modulation in the absence of a static field, at various temperatures spanning the normal-to-superconducting transition. In this particular case, diamagnetic screening first appears at $T \sim 38$ K in the upper left-hand corner of the crystal. Magnetic flux is progressively excluded from the crystal bulk, until the largest part is fully screened at $T = 34$ K. However, the small grain at the bottom is only fully screening at $T = 31$ K. Fig. 3b shows the ac permeability, determined from the luminous intensities $I(r, T) = I(r, T_0) - I(r, T_0 < T_c)/I(r, T_0 > T_c - I(r, T_0 < T_c)$, for four regions indicated in the last panel of Fig. 3a. It is seen that, locally, the crystal shows sharp transitions to the superconducting state. However, a global measurement (e.g. by a commercial magnetometer) would clearly result in a broadened transition.

Local values of the critical current density $j_c$ are obtained from the MO imaging of the largest grains in polycrystalline conglomerates, or from the flux distribution in monolithic crystals, such as depicted in 4a, for PrFeAsO$_{1-y}$ crystal # 7. The magnetic flux distributions in such crystals are characteristic of the Bean critical state. Fig. 4 shows an example of profiles obtained across the central part of crystal # 7 at $T = 11$ K. Due to the relatively large thickness-to-width ratio of the crystal, $d/w = 0.3$, flux profiles resemble straight lines; $j_c \approx 2dB_z/dx$ can be straightforwardly obtained from the flux density gradient.

Resulting values of the critical current density in four areas of PrFeAsO$_{1-y}$ crystal # 7 are shown in Fig. 5, as function of temperature. The inset to the Figure reveals the inhomogeneity of $T_c$ for this particular crystal; the regions in which $j_c$ was measured are also indicated. It is found that $j_c = 3 \pm 1 \times 10^9$ Am$^{-2}$ at the lowest measured temperature. The temperature dependence $j_c(T)$ depends on location. Low $j_c$ areas show a smooth decrease with temperature, whereas regions where $j_c$ is higher feature a crossover in the temperature dependence. Similar behavior is found in all investigated PrFeAsO$_{1-y}$ crystals, see Fig. 6. We shall, in section IV, attribute this behavior to the additive effect of weak collective pinning by oxygen dopant atoms, yielding a strong temperature dependence, and strong pinning, with a weak temperature dependence, coming from disorder of the doping level on the scale of 10 - 100 nm.

Measurements in higher magnetic fields were performed using the Hall array magnetometry technique. Typical results for the self-field, defined as $H_s = B_z/\mu_0 - H_a$, measured on the central part of the top surface of crystal # 7, are shown in Fig. 7. The screening current density is proportional to the difference $\Delta H_s$ measured on the decreasing- and increasing field branches, respectively. A clearly non-monotonous field-dependence of the critical current is observed, with the sustainable current density $j$ rapidly decreasing as the $H_a$ is first increased, followed by an intermediate regime of constant $j$. Fig. 11(a) shows that the low-field behavior, a plateau up to $B^*$, followed by a power-law decrease $\sim B^{3/8}$, is archetypal for a strong pinning contribution to the critical current. However, at intermediate fields, around 0.1 T in Fig. 11(a), $j_c$ does not vanish, but saturates at a value $j_{c SV} \sim 2 - 3 \times 10^9$ Am$^{-2}$ at low temperature. The temperature dependence of the zero-field- and intermediate (constant) values of the critical current are plotted in Fig. 6. One sees that the $j_{c SV}$ contribution is spatially rather more homogeneous, and also that it corresponds to the critical current measured in the most weakly pinning areas of the crystals. Below, we shall attribute this contribution to weak collective pinning by dopant atoms. The strong pinning contribution $j_c(0)$ strongly depends on the location at which it is measured, and it is rela-

![FIG. 4: (color online) (a) Direct MOI of the screening of an dc field by PrFeAsO$_{1-y}$ crystal # 7 (the same crystal as in Ref.$^{27}$), at 7.1 K. Shown are a polarized light image of the crystal; and MOI for $H_a = 300$ Oe, 500 Oe, and the trapped flux in zero field (after the application of 500 Oe). (b) Flux profiles, measured from top to bottom across the central part of this crystal, for increasing values of the applied magnetic field $H_a$, and a temperature of 11 K.](image-url)
The irreversibility field measured from the onset of screening coincides with that determined from the low-field MO data. It therefore does not affect the critical current density at zero field, with parameter values \( n_d = 1.5 \times 10^{27} \text{ m}^{-3} \), \( n_i = 1 \times 10^{27} \text{ m}^{-3} \), and \( f_{p,s} = 0.1 \). Critical current density at \( B_z \approx 300 \text{ Oe} \) were obtained in the same manner as described above. Results for the three regions outlined in the center panel of Fig. 8a are rendered as function of temperature in Fig. 9, together with results obtained by Hall probe magnetometry over the central regions of crystals \#1 and 2. Field-dependent results are shown in Fig. 11(b). The overall behavior recalls that reported in Ref. 25, and is very similar to that observed in PrFeAsO_{1-y}. High critical current areas correspond to a large local contribution of strong pinning, whereas the lower \( j_c^{SV} \) measured at intermediate fields much above \( B^* \) corresponds to the critical current density in the more weakly pinning areas of the crystals. In contrast to PrFeAsO_{1-y}, the strong pinning contribution outweighs \( j_c \) by a factor 2–3. NdFeAsO(O,F) crystal \#2 shows a clear “fishtail” or peak-effect, the corresponding \( B_{on}(T) \) values are plotted in Fig. 12. A hint of a peak-effect is also observed in crystal \#1, but the relative increase of the sustainable current density is much more modest than in the other investigated samples, with data resembling those of Ref. 25. Finally, Fig. 12 shows that the irreversibility field measured from the onset of screening coincides with that determined by the Bean critical state model.33

B. NdFeAsO_{1-y}F_x

Fig. 8a shows magneto-optical images of flux penetration into NdFeAsO_{0.9}F_{0.1} crystal \#1. The sample turns out to be a bicrystal, with a similar spread in \( T_c \) as observed in PrFeAsO_{1-y}. As shown by Fig. 8b, flux distributions inside the crystalline grains are well-described by the Bean critical state model.33 Local values of the critical current density at \( B_{z} \approx 300 \text{ Oe} \) is observed to decay with time, with a typical relaxation rate \( S = (d \ln B_z / d \ln t) \sim -0.05 \) for fields below \( H_{on} \) and \( S \sim -0.03 \) for \( H_a > H_{on} \). As in other studies,14 magnetic relaxation was not observed to affect the low-field MO data. It therefore does not affect the measured temperature dependence of the critical current density in what follows.

As in previous studies on other iron pnictide superconductors,11,14,22,23,25 the local flux density in Tesla fields is observed to decay with time, with a typical relaxation rate \( S = (d \ln B_z / d \ln t) \sim -0.05 \) for fields below \( H_{on} \) and \( S \sim -0.03 \) for \( H_a > H_{on} \). As in other studies,14 magnetic relaxation was not observed to affect the low-field MO data. It therefore does not affect the measured temperature dependence of the critical current density in what follows.

Finally, we turn to higher applied magnetic fields. It is observed that the hysteretic loops open up at a field \( B_{on} \), corresponding to the increase of \( j_c \) at the so-called “fishtail” or peak-effect.11,14,17,20–23,25 The \( B_{on}(T) \) data are collected, together with the irreversibility fields determined from the appearance of a third harmonic component in the ac-response36, in Fig. 12.

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from the onset of a third harmonic response in ac Hall-probe array magnetometry. Moreover, the irreversibility field \( B_{irr}(T) \) for NdFeAs(O,F) and PrFeAsO\(_{1-y}\) crystals with the same \( T_c \) are, within experimental accuracy, identical.

**IV. DISCUSSION**

**A. Weak collective pinning**

We start by analyzing the critical current contribution \( j^{SV}_c \) in terms of the weak collective pinning theory.\(^{13,39,40}\) The vortex lattice order is characterized by the transverse and longitudinal displacement correlation lengths

\[
\langle |\mathbf{u}(R, z) - \mathbf{u}(0, z)|^2 \rangle = r_p^2
\]

\[
\langle |\mathbf{u}(r, L_c) - \mathbf{u}(r, 0)|^2 \rangle = r_l^2,
\]

where \( \mathbf{u}(r, z) \) denotes the deformation field of the vortex lattice at position \( (r, z) \) (with \( z \parallel \mathbf{B} \)), and \( r_p \sim \xi \) is the range of the pinning potential.\(^{41}\) The transverse displacement correlation length

\[
R_c = \left( \frac{\varepsilon_0 \xi}{2 \Phi_{0} \epsilon_0} \right)^{1/2}
\]

can be obtained, without a priori assumptions, from the value of the critical current density. Using the appropriate parameters (Table I), one has, for \( j^{SV}_c (5 \text{ K}) = 3 \times 10^9 \text{ Am}^{-2} \), \( R_c = 40 \text{ nm} \) in single crystalline PrFeAsO\(_{1-y}\), and \( R_c = 56 \text{ nm} \) corresponding to \( j^{SV}_c (5 \text{ K}) \sim 1 \times 10^9 \text{ Am}^{-2} \).

![FIG. 7: (color online) Hysteresis loops of the “self-field”, defined as \( H_s = B_{irr}/\mu_0 - H_a \), as measured with a microscopic Hall sensor in the center of PrFeAsO\(_{1-y}\) crystal # 7, at the indicated temperatures. The values of the onset field \( H_{on} \) are denoted by the vertical black arrows.](image)

in NdFeAsO\(_{0.9}\)F\(_{0.1}\). These values are much smaller than the intervortex spacing at 300 Oe, at which the data in Figs. 5, 6, and 9 were obtained. The pinning-induced displacement of each vortex is thus independent of that of neighboring vortices. In this so-called single vortex pinning limit, one may now estimate the longitudinal displacement correlation length as

\[
L_c = \xi \left( \frac{\sqrt{\frac{\varepsilon_0 \xi}{2 \Phi_{0} \epsilon_0}}}{\frac{\varepsilon_0}{\pi \sigma_{tr} D_r}} \right)^{1/2}
\]

one finds \( L_c \approx 20 \text{ nm} \) and \( 10 \text{ nm} \) for PrFeAsO\(_{1-y}\) and NdFeAsO\(_{0.9}\)F\(_{0.1}\), respectively. This length largely exceeds the spacing of the FeAs planes, which clearly establishes pinning as being in the three-dimensional single-vortex (3DSV) limit.\(^{13,40}\)

From here on, we show that the critical current density in the (1111) iron oxypnictide superconductors can be understood as arising from mean-free path variations induced by the dopant atoms, oxygen vacancies in the case of PrFeAsO\(_{1-y}\), and F ions in the case of NdFeAsO\(_{0.9}\)F\(_{0.1}\). The pinning force of a single defect is expressed as \( f_p \sim 0.3g(\rho_D)\varepsilon_0 \left( \sigma_{tr}/\pi \xi^2 \right) (\xi_0/\xi) \), where \( \sigma_{tr} = \pi D_r^2 \) is the transport scattering cross-section, \( D_r \) is the effective ion radius, and \( g(\rho_D) \) is the Gor’kov function. The disorder parameter \( \rho_D = h\nu_F/2\pi T_{c} l \sim \xi_0/l \),

![FIG. 8: (color online) (a) MOI flux penetration into NdFeAsO\(_{0.9}\)F\(_{0.1}\) crystal # 1, at \( T = 9.1 \text{ K} \). The three frames depict the flux density distribution after the application of an applied field of 20 and 50 mT, and the remanent flux after removal of the 50 mT applied field. (b) Flux density profiles measured across the central part of the crystal.](image)
FIG. 9: (color online) Local values of the critical current density \( j_c \) in the three regions of the NdFeAsO\(_{0.9}\)F\(_{0.1}\) crystal \#1, outlined in the central panel of 9a. Also shown are the values of \( j_c^{SV} \) and \( j_c(0) \) determined for both investigated crystals. The first are compared to Eq. (5) using \( n_d = 1.5 \times 10^{27} \) m\(^{-3} \) and \( D_v = 0.9 \) nm (lower drawn line), while the latter are fit to Eq. (10) with respective parameter sets \( (T_c = 37 \text{ K}, n_i = 6 \times 10^{21} \text{ m}^{-3}, f_{p,s} = 0.1 \varepsilon_0) \) and \( (T_c = 35 \text{ K}, n_i = 2 \times 10^{22} \text{ m}^{-3}, f_{p,s} = 0.1 \varepsilon_0) \).

with \( v_F \) the Fermi velocity, \( l \) the mean free path, and \( \xi_0 \approx 1.35 \xi(0) \) the (temperature-independent) Bardeen-Cooper-Schrieffer coherence length.\(^{13,42} \) The critical current is determined by the fluctuation of the elementary pinning force, \( \langle f^2 \rangle \), and reads\(^{43} \)

\[
j_c^{SV} \approx j_0 \left[ \frac{0.1 n_d D_v}{\varepsilon_\lambda \xi} \left( \frac{\xi_0}{\xi} \right)^2 \right]^{2/3} \tag{5}
\]

\[
x \propto \left[ \frac{\lambda(0)}{\lambda(T)} \right]^2 \left( 1 - \frac{T}{T_c} \right)^\alpha \tag{6}
\]

The numerical factor under the parentheses in Eq. (5) depends on the precise type of scattering.\(^{42} \) Since the temperature dependences \( \lambda(0)/\lambda(T) \) and \( \varepsilon_\lambda(T) \) are known from Refs. 27 and 30 (yielding \( \alpha \approx 2 \) for PrFeAsO\(_{1-y}\) and \( \alpha \approx 1.5 \) for NdFeAsO\(_{0.9}\)F\(_{0.1}\)), one is in the position where a full consistency check of both the magnitude and the temperature dependence of \( j_c \) is possible.\(^{44} \)

In the case of PrFeAsO\(_{1-y}\), Eq. (5), we start from the hypothesis that O vacancies are responsible for the lion’s share of flux pinning. The ion radius \( D_v = 1.46 \times 10^{10} \) m. Inserting this value into Eq. 5 reproduces the low-temperature value \( j_c^{SV} = 3 \times 10^9 \) Am\(^{-2} \) with the single free parameter \( n_d \approx 1.5 \times 10^{27} \) m\(^{-3} \). This nicely corresponds to 0.1 O vacancy per formula unit (half a unit cell of volume 65 Å\(^3\)). Eq. (5) reproduces the low-\( T \) temperature dependence of the critical current density in the high-\( j_c \) regions, and the temperature dependence over the full range from 5 K to \( T_c \) in the low-\( j_c \) regions. The spatially more homogeneous contribution to the critical current density of oxygen deficient single crystalline PrFeAsO\(_{1-y}\) is therefore well-described by pinning by O-vacancies by the \( \delta \kappa \) mechanism.

In the case of NdFeAsO\(_{0.9}\)F\(_{0.1}\), the analysis is hindered by our ignorance of the effective scattering cross-section: doping is through chemical substitution, not oxygen depletion. If one adopts the view that F substitution is at the origin of pinning, one has \( n_d \approx 1.5 \times 10^{27} \) m\(^{-3} \) for our average doping level. To reproduce the value of the measured low-\( T \) \( j_c \approx 1 \times 10^9 \) Am\(^{-2} \) then requires \( \sigma_{tr} = 1.5 \times 10^{-20} \) m\(^2\), corresponding to an effective defect radius of 0.9 Å (this can be compared to the F ion radius of 1.3 Å). The temperature dependence of \( j_c^{SV} \) is again very well described by Eq. (5). It is not quite as strong as in PrFeAsO\(_{1-y}\), an effect that can be attributed to the different \( T \)-dependence of the penetration depth \( \lambda(T) \) nearly perfectly follows \( \lambda^{-2} \sim (1 - t^2) \) and of the anisotropy ratio \( \varepsilon_\lambda \) seems to be nearly independent of temperature in NdFeAsO\(_{0.9}\)F\(_{0.1}\).\(^{40} \)

B. Spatial variations of \( j_c \) and link with doping

Both investigated (1111) compounds show spatial variations of both the critical temperature \( T_c \) and the low-temperature critical current density \( j_c \). It is tempting to correlate the two: knowing the temperature dependence

FIG. 10: (color online) PrFeAsO\(_{1-y}\): critical current versus doping level, as determined from the phase diagram of Ref. 45. Open circles indicate the critical temperature, filled diamonds indicate the critical current density as measured in various locations in the four different crystals of Fig. 6. The dashed and drawn lines indicate the critical current density expected from weak collective pinning by oxygen vacancies, Eq. (5), at \( T = 0 \) and \( T = 5 \) K, respectively (here we suppose that \( \lambda^{-2} \sim T_c \), as in Ref. 47).
of both the superfluid density $\lambda^{-2}$ and the anisotropy ratio, as well as the evolution of the respective $T_c$ vs. doping phase diagrams, Eq. (5) predicts what the dependence $j_c(T_c)$ should be. In the case of PrFeAs$_{1-y}$, our measurements yield sufficient statistics for the expected increase of $j_c$ with $T_c$ to be, indeed, observed. In the considered portion of the phase diagram, the more vacancies are added, the higher $T_c$, but also the stronger the pinning. Fig. 10 shows a compilation of critical temperatures and low-temperature critical currents of all investigated regions in all our PrFeAsO$_{1-y}$ crystals. The experimental data follow the dependence of the low-temperature $j_c$ as this follows from Eq. (5), even though this dependence is weak. The contribution to this dependence via $n_d$, arising from the addition of oxygen vacancies, is actually weaker than the expected contribution from the doping dependence of the the superfluid density, which we have assumed to follow the relation $\lambda^{-2} \propto T_c$. Significant scatter due to the strong pinning contribution remains in Fig. 10, which we shall attribute to the presence of doping inhomogeneity on the $10 - 100$ nm scale.

In the framework of weak collective pinning, the observed spatial variation of $j_c$ in NdFeAs$_{0.9}$F$_{0.1}$ would, if attributed to the macroscopic variation of the dopant atom density, correspond to a variation of the doping level of $x = 0.1 \pm 0.03$, within a given single crystal. The concomitant $T_c$ variation would be from 26 K to nearly 50 K, which is not what is observed by DMO. Moreover, and contrary to the observation in PrFeAsO$_{1-y}$, the critical current density of the investigated crystal is larger in areas with low $T_c$, both as far as different regions of crystal #1 are concerned, as the observed differences between crystals #1 and 2. In the absence of sufficient statistics, we tentatively ascribe this behavior to the presence of strong background pinning.

C. Strong pinning background

As described in section III, the spatial variation of the critical current density in single crystalline PrFeAsO$_{1-y}$ is reflected in the temperature dependence of $j_c$, higher local $j_c$ corresponding to the presence of a break in the temperature dependence. Also, the higher local critical current densities are responsible for the low-field $j_c$ peak observed in Fig. 7, which cannot be explained within the single-vortex collective pinning framework. There must therefore be supplementary sources of pinning, inhomogeneously distributed throughout the samples, with a temperature dependence that is weaker than that of the weak collective pinning described above.

The field dependence of the associated critical current density, a plateau, followed by a power-law decrease $j_c \propto B^{-5/8}$, is in very satisfactory agreement with the theory of strong pinning developed in Refs. 43,48. In the presence of a density $n_i$ of strong pins of size larger than the coherence length, one has

$$j_c(0) = \frac{\pi^{1/2} n_i^{1/2}}{\xi_\lambda} \int_0^{\pi/4} \frac{(f_{p,s} \xi_{ab})^{3/2}}{\xi_0} \left( \frac{B}{B_c} \right)^{3/2}$$

$$j_c(B) \approx \frac{2n_i \xi_0}{\xi_\lambda} \left( \frac{f_{p,s} \xi_{ab}}{\xi_0} \right)^{1/4} \left( \frac{\Phi_0}{B} \right)^{5/8}$$

The crossover field $B^* = 0.74 \xi_\lambda^{-2} \Phi_0 (n_i/\xi_{ab})^{2/5} (f_{p,s} \xi_{ab}/\xi_0)^{6/5}$ is determined as that above which the so-called vortex trapping area of a single pin is limited by intervortex interactions. The identification of the experimental $j_c(0)$ with Eq. (7), and of the power-law decrease with Eq. (8), allows for the determination of the elementary pinning force $f_{p,s}$ of a strong pin from the ratio $\left[ j_c^\text{SV}(B)/dB^{-5/8} \right]/\left[ j_c^\text{SV}(0) \right]^{-2}$. It

![Graph showing critical current versus magnetic field](image-url)
is found that \( f_{p,s}(0) = 2 \times 10^{-13} \text{ N} \) for both investigated compounds, with a temperature dependence coinciding with that of the superfluid density. Hence, we find a measured \( f_{p,s}(0) \approx 0.1 \varepsilon_0 \). The density of strong pins can be straightforwardly estimated from \( B^* : n_i \approx 1 \times 10^{24} \text{ m}^{-3} \) for PrFeAsO\(_{1-y}\), \( n_i \approx 6 \times 10^{21} \text{ m}^{-3} \) and \( n_i \approx 2 \times 10^{22} \text{ m}^{-3} \) for NdFeAsO\(_{0.9}F_{0.1}\) crystals # 1 and 2, respectively.

These data can be compared to the results of TEM observations. The first candidate strong pins are extended (nm-sized) pointlike inclusions or precipitates, such as observed in Fig. 1b. Assuming such defects to be non-superconducting, one would have \( f_{p,s} \sim \varepsilon_0 (D_i/4K_{ab}) \ln \left( 1 + D_i^2/2K_{ab}^2 \right) \). Typical observed defect dimensions are \( D_i \approx 2-5 \text{ nm} \), yielding \( f_{p,s} \sim 0.1 - 1.1 \varepsilon_0 \) at low temperature. Therefore, the smaller defects of radius 2 nm might do the job, were it not that the temperature dependence expected for such voids is at odds with experiment.

Next, the observed undulations of the FeAs layers impose an intermittent bending of vortex lines as these move through the crystal lattice. The necessary force to produce this bending can be estimated as the product of the line tension \( \varepsilon_0^2 \varepsilon_0 \) and the variance \( \delta \alpha^2 \) of the tilt angle; here, \( \alpha \) corresponds to the buckling angle. Such a mechanism would yield the experimental temperature dependence of \( f_{p,s} \), but, at \( 10^{-5} \varepsilon_0 \), grossly underestimates the measured elementary force.

Third, the higher strong pinning critical current density observed for lower doped NdFeAs(O,F) could be linked to the observation of phase coexistence in the underdoped state of this material.\(^9\) Without going as far as invoking the presence of nm-scale magnetically ordered regions in our crystals, the idea of phase coexistence suggests that there are spatial fluctuations of the dopant atom density on the scale of several nm. The ensuing dispersion of weakly superconducting regions with critical temperature \( T_c - \delta T_c \) inside a more strongly superconducting matrix would certainly lead to flux pinning. Its description would be similar to that of non-superconducting precipitates, but with a smaller pinning energy, a vortex passing through an area of lower \( T_c \) gaining only a fraction \( \delta T_c/T_c \) of the condensation energy \( \varepsilon_0/4\xi^2 \). Assuming the condensation energy to be proportional to the critical temperature, the pinning force can be written as

\[
 f_{p,s} \approx \varepsilon_0 (t) \left[ 1 - \left( 1 - \frac{\delta T_c}{T_c} \right) \frac{\varepsilon_0}{\varepsilon_0 (\tilde{t})} \right] \times \left( \frac{D_i}{4\xi_{ab}} \right) \ln \left[ 1 + \frac{D_i^2}{2\xi_{ab}^2} \right]. \tag{9}
\]

with \( t \equiv T/T_c \), and \( \tilde{t} \equiv T_c - \delta T_c \). For small spatial variations of the critical temperature, e.g. \( \delta T_c/T_c \sim 0.05 \) or \( \delta T_c \sim 1.5 \text{ K} \), and \( D_i \sim 5 - 10 \text{ nm} \), Eq. (9) nicely mimics the measured temperature dependence \( f_{p,s}(T) \sim \varepsilon_0(T) \). As shown in Figs. 6, 9, and 11(b), the total critical current density, obtained by summing Eqs. (7) with (9) inserted] and (5),

\[ j_c = j_c^{SV} + j_c^{\ast}. \tag{10} \]

is also in good agreement with experimental observations. One is thus lead to the conclusion that, in addition to the macroscopic inhomogeneity of doping level, there also exists an inhomogeneity on the nano-scale, much similar to that reported by Yamamoto et al. in Ba(Fe\(_{1-y}\)Co\(_{1+y}\))\(_2\)As\(_2\).

However, the doping level modulation, necessarily of the order of the \( T_c \)-variation, \( \delta T_c/T_c \sim 0.05 \), that explains the strong pinning contribution, is far too small to support any claims of phase coexistence in the underdoped (1111) pnictides investigated here. If similar disorder should exist for smaller doping levels, near the superconductivity onset, one would have \( \delta T_c \sim T_c \), and a near certain coexistence of magnetic and superconducting regions. This is a premise that needs further investigation.

For completeness, one may also contemplate surface roughness as a source of flux pinning.\(^{49-51}\) The critical current density is then determined by the force needed to push a vortex line out of a surface trough or across a ridge, and reads, in the limit of small magnetic fields\(^{43,52}\)

\[ j_{cTV} = \frac{\pi \varepsilon_0 \delta d}{\Phi_0 d D} \left( B \approx \frac{\Phi_0}{D^2} \right). \tag{11} \]

Here, \( d \) would be the crystal thickness, \( D \) the spacing between surface defects or troughs, and \( \delta d \) the typical ridge height, that is, the variance of the thickness. In Refs. 49–51, the ratio \( \delta d/D = \sin \theta_c \) is interpreted as the sine of a “contact angle” \( \theta_c \). In the Mathieu-Simon model\(^{49-51}\) the field dependence is expected to correspond to that of the vortex chemical potential, i.e. the equilibrium magnetization. This is not observed. Moreover, if one reinterprets the experimental \( f_{p,s} \) and \( n_i \sim 2/dD^2 \) in terms of surface pinning, one finds a ratio of ridge height to ledge width \( \delta d/D \sim 2 \), for a ledge separation of \( \approx 20 \text{ nm} \). Such a high aspect ratio would mean that the surface defects are located on the crystal edge, since the alternative, cracks on the surface, are not observed. Strong pinning by impurities, located in surface regions only, leads to the same dependences (7,8), but with \( 3 \times 10^{16} \) defects \( m^{-2} \).

D. Fishtail effect and phase diagram

The knowledge of pinning parameters of the (1111) superconductors under study allows one to confront features of the mixed-state \((B,T)\)-phase diagram with theoretical models. In particular, the fishtail effect at \( B_{on}(T) \) was attributed to a crossover in vortex dynamics as, with increasing magnetic field, one leaves the single vortex pinning regime for the bundle pinning regime\(^{53,54}\) or the occurrence of a first order phase transition from an ordered, “elastically pinned” low-field vortex phase, the so-called Bragg-glass,\(^{55}\) to a high field disordered phase characterized by the presence of topological defects\(^{56,57}\).
FIG. 12: (color online) (B, T) vortex matter phase diagram for (1111) iron pnictide superconductors. (Red) Circles indicate measurements on PrFeAsO1−y, while (blue) squares show results on NdFeAsO0.9F0.1. Closed circles show the irreversibility field $B_{irr}(T)$ measured from the onset of a third harmonic response from ac Hall probe magnetometry; open (blue) squares show the screening onset data of Ref. 29. Peak effect onset fields for both compounds are indicated by barred squares (NdFeAsO0.9F0.1) and open (red) circles (PrFeAsO1−y). Dotted lines show the single-vortex to bundle pinning crossover described by Eq. (12), while dashed-dotted lines indicate the order-disorder field described by Eq. (13).

The latter scenario has been unambiguously verified in the high temperature superconductors YBa2Cu3O7−δ and Bi2Sr2CaCu2O8+,17,19 in the cubic superconductor (Ba,K)BiO3,58 in NbSe2,20 as well as in MgB2.21

In the first case, the onset field $B_{on}$ should coincide with the single-vortex- to bundle pinning crossover field $B_{SV}$, determined by the equality of $R_c$ [see Eq. (3)] and the vortex spacing $a_0$:

$$B_{SV} \sim 40 B_{c2} \left( \frac{j_{SV}}{j_0} \right).$$

(12)

Inserting the experimentally obtained $j_{SV}$ into Eq. (12) yields the dotted lines in Fig. 12. Clearly, while the experimental $B_{on}$ data for more strongly pinning PrFeAsO1−y lie below those for more weakly pinning NdFeAsO0.9F0.1, Eq. 12 predicts otherwise. Therefore, even if the peak effect onset lies in the vicinity of the single-vortex to bundle pinning crossover, it cannot be directly associated with it.

On the other hand, the vortex ensemble can undergo a structural transition whereby it lowers its energy by adapting itself more efficiently to the underlying pinning potential, at the expense of the generation of topological defects.55–57 In the absence of a theory for this order-disorder transition of the vortex lattice, a Lindemann-like criterion was developed in Refs. 55,59 and 60 in order to, at least, estimate its position in the $(B,T)$ plane. The Lindemann approach considers that topological defects can be generated when pinning is sufficiently strong to provoke the wandering of vortex lines outside their confining cage formed by the nearest neighbor flux lines. The different results55,60 have been summarized in Ref. 57. In the regime of single vortex pinning, relevant for collective pinning in the (1111) compounds, the position of the order-disorder transition is given by

$$A b_{SV}^{3/5} f_0^{2/5} \left[ 1 + \frac{F_T(t)}{b_{SV}^{1/2} (1 - b_{OD})^{3/2}} \right] = 2\pi c_L^2$$

(13)

where $b_{OD} = B_{OD}/B_{c2}$, $b_{SV} = B_{SV}/B_{c2}$, $c_L = 0.1$ is the Lindeman number, $A$ is a numerical constant, $t = t/T_c$, and $F_T(t) = 2t (G_i/1 - t^2)^{1/2}$. The use of the parameters of Table I, the experimentally measured $j_{SV}$, and $A = 4$ yields the dashed lines in Fig. 12. These show more than satisfactory agreement with the experimentally measured positions of $B_{on}$. We therefore conclude that, most likely, a bulk order-disorder transition of the vortex lattice lies at the origin of the peak effect in (1111) pnictide superconductors. However, more work, especially on vortex dynamics and possible hysteresis associated with the transition, should be performed to ascertain this.

V. CONCLUSION

It is found that superconducting iron pnictide single crystals show significant spatial variations of both the critical temperature $T_c$ and the critical current density $j_c$. Variations of these quantities on the macroscopic scale, from several to several hundred μm, are at the origin of a smearing of globally measured properties, and notably of the width of the superconducting transition. This implies the necessity of local measurements, such as magneto-optical imaging or Hall-probe magnetometry, to extract superconducting parameters. From such local measurements, it is found that the critical current in iron oxypnictide superconductors of the (1111) family of compounds arises from two distinct contributions. The first is weak collective pinning by dopant atoms or vacancies, vortex lines being pinned by the small scale fluctuations of the local dopant atom density. The pinning mechanism is identified as being due to mean-free path variations in the vortex core ($\delta r$ mechanism). This means that dopant atoms should also be effective quasi-particle scatterers. The second pinning contribution manifests itself at low fields. The corresponding critical current contribution can be completely parametrized by the strong pinning theory developed in Refs. 43,48, which means that extended defects are at its origin. An analysis of the magnitude and field-dependence of this strong pinning contribution shows that spatial variations of the doping level on the scale of several dozen to one hundred nm may
be at stake. These variations do not support the possible coexistence of the anti-ferromagnetic metallic and the superconducting phases. Finally, we contend that a bulk order-disorder transition of the vortex ensemble is at the origin of the “fishtail” or peak effect observed in the critical current in sub-T fields.

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