SÍGAME V3: GAS FRAGMENTATION IN POST-PROCESSING OF COSMOLOGICAL SIMULATIONS FOR MORE ACCURATE INFRARED LINE EMISSION MODELING

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ABSTRACT

We present an update to the framework called Simulator of Galaxy Millimeter/submillimeter Emission (SÍGAME). SÍGAME derives line emission in the far-infrared (FIR) for galaxies in particle-based cosmological hydrodynamics simulations by applying radiative transfer and physics recipes via a post-processing step after completion of the simulation. In this version, a new technique is developed to model higher gas densities by parameterizing the probability distribution function (PDF) of the gas density in higher-resolution simulations run with the pseudo-Lagrangian, Voronoi mesh code arepo. The parameterized PDFs are used as a look-up table, and reach higher densities than in previous work. SÍGAME v3 is tested on redshift \( z = 0 \) galaxies drawn from the SIMBA cosmological simulation for eight FIR emission lines tracing vastly different phases of the interstellar medium. This version of SÍGAME includes dust radiative transfer with SKIRT and high resolution photo-ionization models with CLOUDY, the latter sampled according to the density PDF of the AREPO simulations to augment the densities in the cosmological simulation. The quartile distributions of the predicted line luminosities overlap with the observed range for nearby galaxies of similar star formation rate (SFR) for all but two emission lines: \([\text{O I}]63\) and CO(3-2) which are overestimated by median factors of 1.3 and 1.0 dex, respectively, compared to the observed line–SFR relation of mixed-type galaxies. We attribute the remaining disagreement with observations to the lack of precise attenuation of the interstellar light on sub-grid scales (\( \lesssim 200 \) pc) and differences in sample selection.

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1. INTRODUCTION

The physical and chemical state of the interstellar medium (ISM) plays a key role in determining the star formation rate (SFR) of a galaxy and is therefore of immense importance for understanding galaxy evolution. Macroscopic galactic events such as starbursts and mergers create pressure and density waves that determine where and how the giant molecular clouds (GMCs) form in which stars and planets grow (e.g. Colombo et al. 2014; Sun et al. 2018; Chevance et al. 2020; Alves et al. 2020).

Resolved observations of nearby clouds and detailed simulations that track individual cores in GMCs from initial perturbations to final collapse can probe the actual density distribution above the highest density achievable in cosmological simulations. Both observations and numerical work to this effect have determined that the dense gas in molecular clouds (with extinctions $A_v > 1$ and/or $n > 10^3$ cm$^{-3}$) typically has a density probability distribution function (PDF) with a power law tail at the high end set by gravitational collapse (Klessen 2000; Kainulainen et al. 2009; Collins et al. 2012; Girichidis et al. 2014; Burkhart et al. 2015; Schneider et al. 2015; Lombardi et al. 2015; Burkhart et al. 2017; Mocz et al. 2017; Padoan et al. 2017; Alves et al. 2017; Chen et al. 2018). The low-density portion of the density PDF might follow a lognormal shape but this is highly uncertain due to selection effects, completeness, and the influence of stellar feedback (Alves et al. 2017; Chen et al. 2018).

On galactic scales, it becomes too computationally expensive for simulations to model the collapse and fragmentation of each cloud, not to mention the subsequent stellar feedback processes. Instead, parameterizations are used, for example in the cosmological simulations SIMBA (Davé et al. 2019) and IllustrisTNG (Weinberger et al. 2017; Pillepich et al. 2018). In SIMBA, an H$_2$-based SFR recipe is used where the amount of H$_2$ is estimated from the metallicity and local column density following the sub-grid model of Krumholz & Gnedin (2011). In IllustrisTNG, gas with density $n \gtrsim 0.1$ cm$^{-3}$ is allowed to form stars in accordance with the empirically defined Kennicutt-Schmidt relation. Both simulations lack the resolution to track individual stars and instead assume a Chabrier (2003) initial mass function (IMF) for stellar populations formed.

Synthetic observations of simulated galaxies are our most promising way of directly comparing models with observations. Observations of the ISM in galaxies typically target its most effective cooling channels, namely far-infrared (FIR) emission lines. These were discovered by the Kuiper Airborne Observatory (Watson et al. 1984; Stacey et al. 1991; Lord et al. 1996). The subsequent Infrared Space Telescope (Kessler et al. 1996) and Herschel Space Observatory (Herschel hereafter; Pilbratt et al. 2010) showed that the strongest emission lines come from a handful of species, namely neutral and ionized oxygen, singly ionized carbon, and ionized nitrogen, as well as molecular lines such as the CO rotational lines. Together, these species probe all phases of the ISM from GMCs to photon-dominated regions (or photodissociation regions; PDRs), warm neutral medium and hot ionized gas. Existing telescopes such as ALMA, NOEMA, and SOFIA as well as upcoming space and balloon missions (e.g. GUSTO and ASTHROS) provide an ever-growing database of emission line observations of galaxies at all redshifts, requiring detailed modeling of the same lines for their correct interpretation. By taking a snapshot of a hydrodynamic simulation containing gas, stars, and dark matter, line emission can be calculated as a postprocessing step for each cell or particle in the simulation using physically motivated recipes.

All efforts to simulate emission lines have had to determine small-scale values for: 1) the structure and local spectral shape of the radiation field, in particular in the far-ultraviolet (FUV), 2) the structure of gas density, and 3) the local chemistry and level populations. Due to computational constraints, most of these are not calculated with enough precision in the simulation itself, and hence must be derived in postprocessing based on sub-grid models. Below, we summarize the current approaches:

1. For the FUV, the current practice typically involves adopting the strength $G_0$ of FUV interstellar radiation field (ISRF) in the solar neighborhood (Habing 1968) and scaling it by the global SFR of the simulated galaxy compared to that of the Milky Way (e.g. Vallini et al. 2019) to get a galaxy-averaged FUV flux, or by using the local SFR density to get a local kiloparsec-scale FUV flux (e.g. Olsen et al. 2017; Popping et al. 2019). Pallottini et al. (2019) demonstrated the use of on-the-fly radiative transfer for a high-resolution adaptive mesh refinement simulation of a $z \sim 6$ galaxy, and some large cosmological simulations have now also seen on-the-fly radiative transfer,
albeit only from Big Bang through the epoch of reionization and not down to low redshifts (Ocvirk et al. 2016; Wu et al. 2019; Ocvirk et al. 2020). In this work, we introduce a postprocessing radiative transfer calculation for large-box simulations at $z = 0$

2. Retrieving the high-density ($n > 10^4$ cm$^{-3}$) gas during postprocessing of a cosmological simulation is crucial to modeling several FIR lines, as can be seen from the critical densities of typical FIR lines listed in Table 1. This step is typically done by adopting a clumping factor that artificially increases the $H_2$ production (e.g. Narayanan et al. 2008; Gnedin et al. 2009; Davé et al. 2016; Lupi & Bovino 2020), adopting a locally observed molecular cloud mass spectrum together with a derived cloud radius and assumed inner density profile (e.g. Olsen et al. 2015, 2016, 2017; Popping et al. 2019; Inoue et al. 2020), or fragmenting the gas on sub-grid scales following a lognormal density PDF as motivated by Padoan & Nordlund (2011) for isothermal molecular clouds, either using a fixed Mach number (Vallini et al. 2019; Leroy et al. 2017) or calculating the Mach number from local gas properties (e.g. Narayanan & Krumholz 2014; Pallottini et al. 2019). However, the use of the lognormal PDF may be physically unmotivated as evidenced by the lognormal+power law PDF seen in observations and simulations, as described earlier. Vallini et al. (2018) adopted a lognormal+power law PDF for their modeling of CO lines, and we will adopt a similar formalism. In this work, we employ simulations of higher spatial resolution as look-up tables and use analytic relations of density PDFs from Burkhart (2018) to infer the PDF on sub-grid scales in a cosmological simulation.

3. Once the radiation field and density are determined, there are many tools publicly available that simultaneously solve for ionization state, temperature, and line excitation, with some of them being tailored to a specific ISM phase. For an overview of widely used tools to solve for the chemistry and generate line emission in the ISM, see Olsen et al. (2018), which also discusses the limitations of each approach. Most importantly, the chemistry and emission can be solved the simulation or, for a more precise result, with nonequilibrium on-the-fly techniques but at greater computational cost. For an in-depth comparison of the two methods in the case of [C II] and [O I]63 see Lupi et al. (2020). In this work, we use the photoionization code Cloudy (Ferland et al. 2017) to postprocess the simulations to set the shape of the spectrum locally as well as to calculate chemistry and line emission.

As previously mentioned, in addition to inferring the PDF in higher-resolution simulations as described in point 2 above, we also use a theoretical framework to estimate the amount of self-gravitating gas not resolved in the galaxy-sized simulation. In order to alleviate tensions with observations and dense gas models that use a lognormal PDF, Burkhart & Mocz (2019) derive a model of dense gas and star formation based primarily on the presence of a power law tail. The work provides an analytic expression connecting the transitional column density value between lognormal and power law to the width and of the lognormal and the slope of the power law which we will use here (see also Collins et al. 2012; Burkhart et al. 2017; Burkhart 2018).

With this paper, we present a new version of our postprocessing framework Simulator of Galaxy Millimeter/submillimeter Emission (SIGAME; Olsen et al. 2017)

### Table 1. Critical Densities of Important ISM Cooling Lines in the FIR.

| Line | $n_{\text{crit}}$ (cm$^{-3}$) | Origin |
|------|-----------------|--------|
| [C II] | $16^a, 2.4 \times 10^6^b, 4.8 \times 10^4^c$ | All ISM, but mainly PDRs |
| [O I]63 | $4.7 \times 10^5^b$ | PDRs |
| [O III]88 | $510^a$ | H II regions, radiation dominated by OB stars |
| [N II]122 | $310^a$ | Ionized ISM |
| [N II]205 | $48^a$ | Ionized ISM |
| CO(1-0) | $650^c$ | Molecular ISM |
| CO(2-1) | $6.2 \times 10^4^c$ | Molecular ISM |
| CO(3-2) | $2.2 \times 10^4^c$ | Molecular ISM |

Note—CO critical densities were calculated using the spontaneous emission coefficients from the LAMDA database as accessed on 21 Aug 2020 (Schöier et al. 2005), using a temperature of 100 K and typical collision cross section of $10^{-15}$ cm$^{-3}$. The [C II] critical densities are from Goldsmith et al. (2012), calculated at a temperature of 500 K. The remaining critical densities are from Madden et al. (2013) at 300 K.

*a* For collisions with electrons.

*b* For collisions with hydrogen atoms.

*c* For collisions with H2 molecules.
to model FIR/millimeter line emission in particle-based hydrodynamic simulations, and test it on a large sample of emission lines for comparison with observations. Section 2 describes the new structure of sīGAMe in detail and lists the updates made since the previous version. Section 3.1 describes the test sample of simulated galaxies used, and the rest of Section 3 tests the code under different assumptions and makes a rough comparison with observations and the previous version of sīGAMe. Section 4 discusses the results and provides caveats for using this method. Finally, we conclude in Section 5.

Throughout this paper, we adopt a flat cold dark matter cosmology with cosmological parameters $\Omega_m = 0.693$, $\Omega_b = 0.307$, and dimensionless Hubble parameter $H_0 = 0.678$ (Planck Collaboration et al. 2016).

2. SĪGAME VERSION 3

sīGAMe derives FIR/millimeter line emission of simulated galaxies by postprocessing a particle-based cosmological hydrodynamics simulation. We currently use particle-based simulations, but grid-based simulations are in principle also usable with the new framework presented here. Figure 1 provides a quick look at the overall structure of sīGAMe version 3. ? adapted version 2 of sīGAMe to apply it to the SIMBA simulation for the first time to study the [C II] luminosity function at $z = 6$. With this version 3, the main updates are:

- Radiative transfer of stellar FUV emission through dust. sīGAMe v2 used a library of STARBURST99 (Leitherer et al. 2014) synthesis models for stellar populations to derive the local FUV field, without taking into account the potentially important effect of dust absorption. In sīGAMe v3 a full dust radiative transfer calculation is performed using the three-dimensional (3D) radiative transfer code SKIRT\(^1\) (Camps & Baes 2020) and the actual dust-to-metal (DTM) ratios from the cosmological simulation if available.

- Fragmentation of the gas on sub-grid scales. In previous versions of sīGAMe, gas particles from cosmological simulations were divided into a diffuse gas phase and a dense one, the latter being further divided into spherical GMC-like structures with masses $> 10^4 M_\odot$. With the new version of sīGAMe, gas particles are first distributed on an adaptive grid with SKIRT and then fragmented according to the local gas and SFR volume densities using the output from a high resolution simulation, and thereby avoiding the assumption of spherical clouds.

- High-resolution thermochemistry of the ISM. As in previous versions of sīGAMe, we use the photoionization code CLOUDY (this time version 17.02) to calculate the chemical and thermal state of the gas and the resulting line emission. However, because of the decision to fragment the gas to smaller mass and size scales, we have moved to using the GRID COMMAND feature of CLOUDY, allowing for a look-up table of higher resolution.

The following four subsections describe in detail the algorithms that are applied within each of the four steps indicated in Figure 1:

2.1. Dust attenuation with SKIRT (step 1)

We use the 3D radiative transfer code SKIRT (Camps & Baes 2020) to calculate the local dust-attenuated ISRF. SKIRT uses information on the dust and stellar distribution in the galaxy simulation to inform a Monte Carlo algorithm on how to emulate the relevant physical processes including scattering, absorption, and emission of photons as they pass through the interstellar dust. For the stellar component (“SourceSystem” in SKIRT), an IMF similar to that used in the galaxy simulation is chosen, and the stellar emission is set to match the Binary Population and Spectral Synthesis (BPASS v2.2.1) models according to the age and metallicity of each star particle (Eldridge et al. 2017; Stanway & Eldridge 2018).

SKIRT requires radiative smoothing lengths around each stellar particle’s position to spread out the launch locations of the photon packets around that position. If such a smoothing length is not available in the simulation, sīGAMe will calculate one that scales linearly with stellar mass and spans 100–300 pc. Often, SKIRT divides the dust medium into cells of sizes much smaller than 100 pc, but we note that the gravitational smoothing lengths of cosmological simulations are typically much larger (of the order of 1 kpc). Therefore, although SKIRT inserts a lot of cells to ease the radiative transfer calculation, adjacent cells often have similar densities. The choice of scaling the radiative smoothing length to between 100 and 300 pc was made after having tested two extreme cases: (a) stellar smoothing lengths of 10 pc and (b) stellar smoothing lengths of 1000 pc. In case (a) the stellar radiation field ends up being concentrated in point sources and in the case (b) the stellar radiation field creates artificial “rings” around the original stel-
Figure 1. Flow chart illustrating the structure of SIGAME v3.

This dust mixture contains two families of dust particles: amorphous silicate and amorphous hydrocarbon (we refer to Jones et al. 2017 for more detail). The post-processing with SKIRT returns a spectrum for each cell of each galaxy on an oct-tree adaptive grid. The rest of SIGAME works on this grid structure, for which gas densities are calculated with the SWIFTSimIO package (Borrow & Borrisov 2020), and all other properties are inherited from the nearest fluid element or gas particle in the galaxy simulation.

2.2. Attenuation by intervening gas with Cloudy (step 2)

In addition to being attenuated by dust grains, interstellar light from stars is also absorbed by gas, in particular in the hydrogen-ionizing regime at photon energies above 13.6 eV. With SKIRT a spectrum is generated in each cell that has been attenuated by dust only, which tends to absorb radiation in the FUV at 6–13.6 eV (Gnedin et al. 2008). In order to account for the additional attenuation by gas, we run a suite of CLOUDY models for a fixed luminosity source, over a range of total hydrogen column densities. For the luminosity source, an unobscured stellar spectrum of a stellar population of age 1 Myr and solar metallicity, scaled to a luminosity of $10^6 L_\odot$, using the same BPASS v2.2.1 tables as those used in the modeling with SKIRT. The stellar spectrum

2 For more detail, we direct the reader to an issue on the SKIRT GitHub site (SKIRT repo 2019), in which we discussed this question at length with SKIRT developer Peter Camps, and where plots can be found of the various options tested.
Figure 2. Transmitted spectra for a set of CLOUDY 1D slab models with hydrogen density $1 \text{ cm}^{-3}$ and solar dust and metal abundances. The OIR and FUV photometric bands that we use to derive the OIR/FUV flux ratio are indicated with shaded regions, and a vertical dashed line highlights the 13.6 eV ionization potential of hydrogen. The luminosity source used is a combination of the local ISRF continuum together with the spectrum of a BPASS v2.2.1 binary star model with age $10^6 \text{ Myr}$ and solar metallicity and with a bolometric luminosity normalized to $10^6 L_\odot$. The different spectra were created by changing the column density of the 1D slab from $\log N_H = 17$ to $\log N_H = 24$. 

is added to a background continuum spectrum corresponding to the observed local ISM ISRF as available with the “table ism” command in CLOUDY. For these models, we keep the metallicity at $1Z_\odot$ and maintain the dust size distribution and abundance to that appropriate for the ISM of the Milky Way as given by the CLOUDY “grains ISM” command. The latter includes both a graphitic and a silicate component and generally reproduces the observed overall extinction properties for a ratio of extinction per reddening of $RV \equiv A_v/E(B-V) = 3.1$ (we refer to the CLOUDY manual for details). We use the local ISM abundance table of CLOUDY, which is a mean of the warm and cold phases of the ISM from Cowie & Songaila (1986) and Savage & Sembach (1996). In these CLOUDY models, and all other CLOUDY models in this work, the cosmic microwave background at $z = 0$ is included as an additional blackbody radiation field. By changing the column density at which CLOUDY stops the calculation, a set of transmitted spectra of different shapes are produced containing the effects of different amounts of dust and gas absorption as shown in Figure 2.

From the shape of the spectra in Figure 2, we quantify the effect of dust absorption as the ratio between optical-to-near-infrared (OIR; 0.5–2 eV) flux and FUV flux (red and teal shaded regions in Fig.2). We can now match the derived OIR/FUV flux ratio with that of SKIRT in each simulation cell to translate the dust extinction into an average column density of gas that the stellar light has passed through, and thereby complete the shape of the incident spectrum (not the normalization) to be used for the final CLOUDY grid described in Section 2.4. The inclusion of absorption by gas in this way is not an exact solution because we are essentially approximating the effect of several luminosity sources and column densities taken into account by SKIRT with a single luminosity source and one column of gas and dust in CLOUDY. We do this because there is no clear way of recovering the exact path of each photon packet ejected by SKIRT. Furthermore, this method assumes a constant DTM ratio (fixed at roughly 0.5 here) and uses a single metallicity for all the intervening gas. Finally, we note that the chosen stellar population sets the X-ray portion of the spectra in CLOUDY which is further attenuated by gas and dust as seen in Fig.2. Yet this part of the spectrum could look very different for a stellar population of different age and metallicity, and the intensity of X-rays could potentially affect the emission line flux (see Vallini et al. 2018, for a study on CO emission from high-$z$ active galactic nuclei (AGNs)).

2.3. Gas fragmentation (step 3)

Due to the limited resolution of cosmological simulations, the individual cells typically do not contain densities higher than $\sim 10 \text{ cm}^{-3}$ (see Appendix C for the gas and SFR density distributions in one of the simulated galaxy samples used to test SIGAME in the following sec-
tions). However, all the FIR emission lines considered here can or will only be excited at much higher densities, as can be seen from the critical densities listed in Table 1. In order to perform the dust radiative transfer, Skirt introduces cells of smaller size than those in the source simulation, but this procedure does not increase the density of the gas.

To mitigate the lack of resolution in density, this version of SIGAME turns toward simulations made at much higher spatial resolution in order to use them as look-up tables that can help describe the fragmentation of the gas on sub-grid scales. In principle, the user can import their simulation of choice, but for the purpose of testing SIGAME in this paper we chose the high-resolution data from a simulation performed with the Voronoi mesh code arepo (Springel 2010) of an interacting M51-like galaxy model (Tress et al. 2020). The simulation (hereafter described as arepo-M51) reached subparsec resolution in dense gas and allowed for an analysis of the formation and destruction of GMCs, which showed that the evolution of GMCs depends only weakly on galaxy–galaxy interactions.

2.3.1. The arepo-M51 simulation

For details on the simulation setup we refer to Tress et al. (2020), summarizing here only the components of relevance to this project. The arepo-M51 simulation was designed to be able to resolve and study GMCs in the context of a galaxy interaction. The simulation setup includes a time-dependent, nonequilibrium, chemistry network tracking hydrogen and CO chemistry, and follows star formation and feedback processes, reaching subparsec resolutions at densities $n \gtrsim 100$ cm$^{-3}$ (see Fig. 3 of Tress et al. 2020). The calculations were executed using arepo, a magnetohydrodynamic (MHD) code using an approximate Riemann solver coupled to an oct-tree gravity solver, from which only the hydrodynamic capabilities were used (Springel 2010; Weinberger et al. 2020). At each time step the code constructs the Voronoi grid given a set of mesh-generating points that are constrained to move following the local velocity of the fluid. This pseudo-Lagrangian moving-mesh technique is naturally adaptive, allowing for high dynamic range on spatial scales down to the substructure of GMCs.

The galaxy model and the interaction with a companion were adjusted to resemble the M51 system, and the chemical network followed the cooling and self-shielding of molecular gas from foreground interstellar radiation. This allowed the formation of GMCs where runaway collapse leads to star formation (SF). Dense, gravitationally bound, and collapsing gas is accreted onto collisionless sink particles that abstract the last stages of the SF process to a sub-grid model due to the limited resolution of even this higher-resolution simulation.

At gas densities $\rho_\text{c} > 10^{-21}$ g cm$^{-3}$ ($n_\text{H} \gtrsim 600$ cm$^{-3}$) the gas is tested to determine whether it is bound and collapsing, and if so a sink particle is created. Dense gas with $\rho > \rho_\text{c}$ that comes within an accretion radius of 2.5 pc will then be accreted by the sink particle if bound to it. Given these densities and sizes, the sink particles represent small stellar (sub)clusters. At these scales SF is still fairly inefficient, so only 5% of the accreted gas mass is converted into stars. In this sense every sink particle consists of a stellar component and a gas component. Each stellar component is modeled as a stellar population whose initial stellar masses are drawn from an input Kroupa (2001) IMF. The massive stars drawn are evolved based on a simple stellar evolution model Maeder (2009) and at the end of their lifetime they produce a supernova (SN) feedback event, disrupting the clouds and closing the ISM lifecycle. Note that this approach is different from the traditional star particle approach of cosmological simulations, as we explicitly consider the gravitational binding of the gas to model ISM fragmentation and then include subsequent gas accretion.

The gas component trapped within the sink particle is progressively ejected and re-added to the gas phase with every SN event. After the last SN of a particular sink, the sink particle includes only stellar mass and is converted to a different particle type that represents an old stellar population. By drawing randomly using Poisson sampling from the IMF, it could occur that in particular cases no massive star is generated within the sink. In that case, after a trial period of 10 Myr, the gas component is ejected from the sink without an SN event and the sink is then converted to an old stellar population particle. Significant approximations of the arepo-M51 simulation include the lack of early stellar feedback such as winds, jets, and ionizing radiation and the absence of magnetic fields.

2.3.2. Parameterizing the density PDF

The arepo-M51 simulation contains starbursting regions as well as regions with hardly any ongoing star formation. The question we pose is: how does the gas density PDF change from one region to another and can we parameterize it for use in a cosmological simulation of much lower resolution? To investigate this, we divide the arepo-M51 simulation volume into cubes of 200 pc on a side and calculate the gas density PDF within each cube. The region size of 200 pc was chosen in order to represent typical Skirt cell sizes, and at the
Figure 3. Volume-weighted gas density PDFs from the selected AREPO-M51 run and fitted functions constructed as described in Section 2.3. Each panel indicates a specific bin in gas density, $\langle n_H \rangle_V$, and SFR volume density, $\langle n_{\text{SFR}} \rangle_V$. The gray contours correspond to the 1-σ spread around the mean volume-weighted PDF (dashed teal curve) made from AREPO gas cells within regions of (200 pc)$^3$. The solid teal curves are lognormal+power law fits to the mean PDF. A vertical dashed red line indicates the critical density above which sink particles may form, at which point the density PDF from gas cells alone is no longer comprehensive. The orange dashed curves account for the dense gas in sink particles by adding this mass at the high densities in the form of a modified power law slope, and the orange solid curves are the resulting lognormal+power law fit to the new distribution. The units for $\langle n_H \rangle_V$ and $\langle n_{\text{SFR}} \rangle_V$ are in cm$^{-3}$ and $M_{\odot}$ yr$^{-1}$kpc$^{-3}$, respectively.

Due to the spread in PDFs, as indicated with gray areas in Figure 3, we cannot just interpolate between PDFs. Instead, we make a parametric fit, such that the fit parameters depend on $\langle n_H \rangle_V$ and $\langle n_{\text{SFR}} \rangle_V$. For the parametric fit, we build on previous work showing that the density distribution of a collapsing cloud can be approximated by a lognormal with a power law tail. As discussed in the Introduction, both observations and simulations show that the density field of an isothermal star-forming cloud is well approximated by a lognormal distribution at low density and a power law distribution at high density. Burkhart (2018) describes the resulting...
PDF as
\[ p_{LN+PL}(s) = \begin{cases} N \frac{1}{\sqrt{2\pi}\sigma_s} e^{-\frac{(s-s_0)^2}{2\sigma_s^2}}, & s < s_t, \\ Ne^{-\alpha s}, & s > s_t, \end{cases} \]
where \( N \) is the normalization constant, \( \sigma_s \) is the standard deviation of the lognormal, \( \alpha \) is the power law slope, \( s_0 \) is the mean logarithmic overdensity, and \( s \) is the logarithmic overdensity
\[ s \equiv \ln\left(\frac{\rho}{\rho_0}\right), \]
where \( \rho_0 \) is the volume-averaged density of the entire cloud. The transition density, \( s_t \), above which the distribution approximates a power law, was shown by Burkhart (2018) to relate to the lognormal width \( \sigma_s \) and power law slope \( \alpha \) as
\[ s_t = (\alpha - 1/2)\sigma_s^2. \]

In Figure 3 a fit is made to all mean PDFs by combining a lognormal function with a power law at the high-density end, keeping \( \sigma_s \) and \( \alpha \) as free parameters.

However, this fit does not take into account gas mass locked in sink particles. The gas in sink particles where no SN has exploded will be dense and distributed in relatively undisturbed GMCs, while gas in other sink particles with supernova remnants (SNRs) has already been at least partly dispersed in the surrounding ISM due to SN feedback. In order to account for the dense gas mass in sink particles, we divide the sink particles into two categories:

- **Category I sink particles** contain dense, cold gas that creates stellar populations with time, but no SN explosions. Here, we expect the gas to be relatively undisturbed and we count all gas mass in the particle as dense gas following a power law density PDF regardless of the sink particle age. The percentage of sink particles in this category is only 0.13%.

- **Category II sink particles** contain dense, cold gas that has formed or will produce at least one SN. Due to feedback from the massive stars that eventually produce SN explosions, a GMC will not survive for long in this environment. In a study looking for OH(1720 MHz) masers in the inner Galaxy, Hewitt & Yusef-Zadeh (2009) found that dense gas interacts with only 15% of SNRs. Considering that SNRs are visible only during the first \( \sim 0.1 \) Myr of their lifetime and assuming that SNe occur at a roughly constant rate after the first SNe go off, we can convert the SNR number fraction of 15% into an upper age limit. We count gas in sink particles with SNRs as being dense gas only if the sink particle age since the first SN exploded is less than 15% of the longest SNR lifetime. The first SNe, created by the most massive stars, are expected to begin exploding at a sink particle age of \( \sim 3 \) Myr (e.g. Yungelson et al. 2008). The percentage of sink particles in this category is 22.7%.

We count the internal gas mass of the remaining sink particles as diffuse gas that would already have been dispersed by feedback if ionization and winds were included. As sink particles accrete more mass than forms into stars, there is a maximum mass limit of \( \sim 2 \times 10^5 \) M\(_\odot\) above which they are not allowed to accrete further and instead form a new sink particle. This retains nominal resolution in the collisionless particles instead of having single particles with anomalously high mass. Figure 4 illustrates the selection criteria and the distribution in sink particle ages and total current gas masses (total sink mass – sink stellar mass). The older the sink particles, the more likely it is that stars have formed and the gas has been used up or dispersed. This outweighs the additional mass from accretion over time. A main branch can be seen of sink particles that start out with the maximum mass and begin to reduce in gas mass after a period of 3 Myr when SNe start to disperse the gas (Category II sink particles by the definition above). Another branch is of sink particles that ran out of gas, many of which are Category I particles that will never produce an SN.

**Figure 4.** Distribution of sink particle gas mass and age in AREPO-M51. The teal circles and teal shaded area illustrate the selection criteria of Category I and II sink particles, respectively, as described in Section 2.3.
The additional sink gas mass is expected to change only the high-density portion of each PDF, because it has already passed the accretion density threshold of $\rho_c = 600 \text{ cm}^{-3}$. We first attempt to accommodate the sink gas mass by iterating on the power law slope until enough additional mass has been added. This method results in the orange dashed curves in Figure 3, while the orange solid curves are combined lognormal and power law fits made to the new distributions.

The resulting fits, shown with orange curves in Figure 3, are used as look-up tables for each cell in the Skirt output, by interpolating in $\langle n_H \rangle_V$ and $\langle n_{\text{SFR}} \rangle_V$. The corresponding sonic Mach numbers, $M_s$, for each fit can be estimated from $\sigma_s$ through (Padoan et al. 1997):

$$\sigma_s^2 = \ln(1 + b^2 M_s^2).$$

Adopting a turbulent forcing parameter of $b = 1/3$, our density PDFs display Mach numbers from 7 to 27. For cell densities below the minimum grid point in the Arepo-M51 look-up tables, we adopt a single, narrow lognormal PDF corresponding to a Mach number of 1 and $b = 1/3$ (Federrath et al. 2008) without the power law tail. All PDFs are cropped to the density range from $n_H = 10^{-4} \text{ cm}^{-3}$ to $n_H = 10^7 \text{ cm}^{-3}$.

### 2.4. FIR line emission with Cloudy (step 4)

The final step of simba v3 is to derive the line emission, having gathered all the necessary information by post-processing the simulation. To this end, we use a library of one-zone Cloudy models that span the parameter ranges listed in Table 2. As mentioned in Section 2.2, the column densities (log $N_H$) in Table 2 are not actual column densities in the simulations, but a parameter used to set the shape of the spectra. For each value of the $F_{\text{FUV}}$ flux, the cosmic ray ionization rate $\xi$ is scaled as

$$\xi = (F_{\text{FUV}}/G_0)\xi_0,$$

where $\xi_0 = 10^{-16} \text{ s}^{-1}$ is taken as the average Milky Way value (Indriolo et al. 2007) and the solar neighborhood FUV flux $G_0 = 1.6 \times 10^{-3} \text{ erg cm}^{-2} \text{ s}^{-1}$ (Habing 1968). Exploring all combinations of the parameters listed in Table 2, leaves us with 129,600 Cloudy one-zone models.

The one-zone Cloudy models must now be sampled according to the gas density PDFs found in Section 2.3, such that each combination of $\langle n_{\text{SFR}} \rangle_V$ and $\langle n_H \rangle_V$ in the galaxy simulations corresponds to a density PDF-weighted sum of the 12 different one-zone Cloudy models along the log $n_H$ axis that correspond to that region’s other parameters (log $Z$, log $N_H$, log $F_{\text{FUV}}$ and log DTM). For this step, six grid points in $\langle n_H \rangle_V$ (from $10^{-4}$ to $10^2 \text{ cm}^{-3}$) and four grid points in $\langle n_{\text{SFR}} \rangle_V$ (from $10^{-2.5}$ to $10^{0.5} \text{ M}_\odot \text{ yr}^{-1}$) are used. For each combination of $\langle n_H \rangle_V$, $\langle n_{\text{SFR}} \rangle_V$ we take the gas density PDF that comes closest in terms of both values, and shift the center of the lognormal to exactly match $\langle n_H \rangle_V$. This shift is performed to ensure that the PDFs generated are not only centered on the six chosen $\langle n_H \rangle_V$ grid points, but can fill out the density space and generate a smooth total PDF as shown in Fig. 7. The sampling of one-zone Cloudy models is carried out for all combinations of $N_H$, $F_{\text{FUV}}$, $Z$, and DTM ratio, leading to a look-up table of 259,200 different combinations of one-zone Cloudy models, with one such table for each spectral line considered.

#### 2.4.1. User-defined sub-grid attenuation function

The Skirt calculation yields the average ISRF on scales similar to the resolution of the original cosmological simulation and hence parsec-size substructures are not taken into account by Skirt. As a way of compensating for this lack of resolution, we have included in the framework an optional user-defined function to add extinction on sub-grid scales. In practice, this is done by generating a one-zone Cloudy grid as described in Section 2.4 but for which the incident spectra were attenuated using the “extinguish” command in Cloudy. This command diminishes the incident spectrum with a simple power law corresponding to an intervening slab of gas of fixed column density, which is set to $10^{24} \text{ cm}^{-2}$ here.

For the Simba simulations at hand, we test the framework with a very simple extinction function, which only adds extinction to Cloudy grid cells of density above $10^2 \text{ cm}^{-3}$. When constructing the look-up table by sampling the gas density PDFs (Section 2.3), these extinguished models can now be sample for a certain range in density ($\xi$ not being modified). For instance, all one-zone models with densities above a certain threshold can be assigned the attenuated spectrum to account for un-

### Table 2. Parameters for the One-zone Cloudy Models.

| Model Parameter | Min. value | Max. value | Step Size |
|-----------------|------------|------------|-----------|
| log $n_H$ [cm$^{-3}$] | -4 | 7 | 1 |
| log $Z$ [$Z_\odot$] | -2 | 0.5 | 0.5 |
| log $N_H$ [cm$^{-2}$] | 17 | 22 | 0.5 |
| log $F_{\text{FUV}}$ [$G_0$] | -7 | 4 | 1 |
| log DTM ratio | -2 | -0.2 | 0.2 |
resolved dense and shielded substructures. This procedure roughly mimics a scenario in which high-density gas regions are the most shielded from ionizing photons. In the following Sections we will compare the results with and without this additional function.

3. TESTING OF THE CODE

3.1. The $z = 0$ simulated galaxy sample

We apply SIGAME to a simulated galaxy sample from the SIMBA cosmological galaxy formation simulation (Davé et al. 2019). The SIMBA simulations are run using the meshless finite-mass hydrodynamics technique in the GIZMO-N-body plus hydrodynamics code (Hopkins 2015, 2017). The main SIMBA run evolves $1024^3$ gas elements and $1024^3$ dark matter particles within a $100 h^{-1} \, \text{Mpc}$ volume (SIMBA-100) from $z = 249 \to 0$. To improve the dynamic range and test resolution convergence, we also use a higher-resolution run with $512^3$ gas elements and $512^3$ dark matter particles within a $25 h^{-1} \, \text{Mpc}$ volume (SIMBA-25).

SIMBA includes a range of sub-grid models for galaxy formation physics, including $\text{H}_2$-based star formation, two-phase kinetic galactic winds, torque-limited and Bondi black hole accretion, three types of AGN feedback, and a sub-grid model to form and destroy dust during the simulation run (Li et al. 2018, 2019). The galaxy properties in SIMBA have been compared to various observations across cosmic time and shown to provide reasonable agreement (e.g. Thomas et al. 2019; Appleby et al. 2020; Lower et al. 2020; Rodríguez Montero et al. 2019). For more details we refer to Davé et al. (2019).

We extracted samples of galaxies from the $z = 0$ snapshots of SIMBA-100 and SIMBA-25 using the CAESAR galaxy and halo catalog generator, which identifies galaxies using a six-dimensional friends-of-friends algorithm applied to dense gas ($n > 0.13 \, \text{cm}^{-3}$) and stars (Thompson 2015). Before making any selection cuts, a total of $49,215$ and $2463$ galaxies were found by CAESAR for SIMBA-100 and SIMBA-25, respectively. To ensure we have a reasonably well-resolved gas distribution within the galaxy, we only consider galaxies with $> 300$ gas elements in both simulation boxes, corresponding to a gas masses of at least $5.6 \times 10^9 \, M_\odot$ and $0.7 \times 10^9 \, M_\odot$ in SIMBA-100 and SIMBA-25, respectively. For comparison the mass resolution of the AREPO-M51 simulation, which will be used to fragment the gas as described in Section 2.3, is a few solar masses. From these we select a test sample of $400$ galaxies from SIMBA-100 and another sample of $240$ galaxies from SIMBA-25. The samples were selected to span a wide range in stellar mass, SFR, and gas mass. Only galaxies found to have nonzero mean SFR over the past $100$ Myr were included.

Figure 5 shows the positions of the SIMBA-100 and SIMBA-25 galaxy samples in the SFR–$M_*$ space. The distribution of all SIMBA-100 and SIMBA-25 $z = 0$ galaxies identified with CAESAR and within the axis limits is shown underneath with logarithmic hexbin contours. The agreement with observations by Salim et al. (2018) is generally good, though SIMBA overestimates the SFR over the range $M_\ast \sim 10^{9.5} – 10^{10} M_\odot$ (see discussion of this in Davé et al. 2019). Overall, SIMBA reproduces the observed SFR–$M_*$ distribution fairly well, both in terms of the main sequence and the quenched fractions (Davé et al. 2019), as well as the bimodality in specific SFR (Katsianis et al. 2020).

For our SIMBA-100 sample, hydrogen densities range from $0.5$ to $66 \, \text{cm}^{-3}$ and SFR-weighted mean metallicities $(Z)_{\text{SFR}}$ span $0.1–1.9 \, Z_\odot$. By weighing the metallicity by SFR, we are approximating the metallicity that would be observed using nebular emission lines since these lines primarily trace star-forming regions. Global galaxy properties such as stellar mass, gas mass, SFR, $(Z)_{\text{SFR}}$, and radius can be found in Table 4 together with...
Figure 6. Examples of three SIMBA-25 galaxies going through step 1 of SIGAME, where stellar light is propagated, attenuated, and re-emitted by dust grains using the radiative transfer code SKIRT. Left column: surface density maps of the total gas mass in SIMBA. Center column: positions and ages of all stellar population particles with ages below 1 Gyr. The sizes of the stellar circles scale with stellar population mass. Right column: maps of observed FUV (6–13.6 eV) flux derived with SKIRT as observed from a distance of 10 Mpc, showing increased FUV flux in areas close to young stellar populations and attenuation by regions of dense gas.
their line luminosities in Table 5 in Appendix A and online.

Figure 7. Examples of density PDFs for the same three SIMBA-25 galaxies as shown in Figure 6, in the same order. Each panel compares the density PDF of the simulation, after regridding the particle data to a grid format with SKIRT (solid histogram), the density PDF using the parameterized PDF from AREPO-M51 (dashed line), and the density PDF when adopting a lognormal of Mach number 10 for each gas cell (dotted line).

Figure 6 illustrates the outcome of modeling and propagating the stellar light with SKIRT in step 1 of SIGAME (see Section 2.1). SKIRT outputs the radiation in cells with sizes ranging from 19 pc to 6.3 kpc, and a mass-weighted distribution in cell sizes that peaks at ~200 pc (for the SIMBA-100 galaxies). For the purposes of this paper, we found that a total of 10^8 photons per galaxy was enough to give stable results, corresponding to more than ~2, 500 photons per star particle. See Appendix B for a test increasing the number of photon packets to 10^9 that resulted in a negligible change in total FUV luminosity and FUV flux distribution. For the dust component (“MediumSystem” in SKIRT), we directly use the dust masses that are calculated on-the-fly in SIMBA (Li et al. 2019). The resulting total infrared (3–1100 µm) luminosities span from 2.41 × 10^7 L⊙ to 2.73 × 10^{11} L⊙ and FUV (6–13.6 eV) luminosities from 5.78 × 10^7 L⊙ to 1.09 × 10^{10} L⊙ using the SIMBA-100 dust masses directly. The mass-weighted metallicities of our model galaxies range from 0.02 to 1.9 Z⊙ for the SIMBA-100 sample, so we set the metallicity of intervening gas to 1 Z⊙ in step 2 of SIGAME (see Section 2.2).

After step 3 of SIGAME (see Section 2.3), we can construct galaxy-wide density PDFs, and examples for the same galaxies as in Figure 6 are shown in Figure 7. The original density PDF in the cell data from SKIRT (solid line) is compared to the derived PDF adopting a single lognormal with Mach number 10 and forcing parameter b = 1/3 versus the approach described in Section 2.3 in dotted and dashed lines, respectively.

Fig 8 shows moment0 maps of CO(1-0), [C II] and [O III]88 emission constructed for the same three galaxies from SIMBA-100 shown in Figure 6, using the output from completing step 4 of SIGAME (see Section 2.4). The output data cube from SIGAME contains spatial information, cell sizes, and cell luminosities that were combined to derive the surface brightness of each pixel in the final image, weighting each cell by its volume filling factor within the column covered by each pixel³. We note that the calculation of the moment0 maps assumes an ISM fully transparent to the FIR line emission, an assumption that might not hold for shorter wavelengths. Some expected differences in how the emission lines trace the ISM can be observed, such as the preference for [C II] to arrive from PDRs near star forming regions compared to the broader CO(1-0) emission, and the relatively concentrated [O III]88 emission restricted to H II regions experiencing harder radiation fields from young stars. The more concentrated [C II] and [O III]88 emission relative to the CO(1-0) is also reflected in slightly smaller half-

³ https://github.com/jaymotka/moment0_maps
light radii compared to the CO(1-0) maps as illustrated with green dashed circles.

### 3.2. sGAME runs

In order to compare different assumptions in the sub-grid process, we perform four different runs on the same $z \sim 0$ sample from the SIMBA-100 box as well as one run on galaxies selected in the SIMBA-25 box. The names of the different runs are listed in Table 3. In the first run (100Mpc_M10 in Table 3), we report the line luminosities that sGAME returns when the density fragmentation is carried out the “traditional way” with a single lognormal density PDF corresponding to a Mach number 10 and a forcing parameter of 1/3. A value of 10 for the Mach number is supported by observations of clouds in the solar neighborhood with typical sound speeds of 0.2–0.3 km s$^{-1}$ and velocity dispersions of several km s$^{-1}$ (see, e.g. Goldreich & Kwan 1974; Kainulainen & Tan 2013; Hennebelle & Inutsuka 2019). Next, we applied sGAME v2 to the same set of galaxies, using the modifications to the code described in [7] together with a new CLOUDY grid at $z = 0$ (100Mpc_SIGAMEv2). The next simulation run adopts the new gas fragmentation scheme described in this paper, and will be referred to as our “default run” (100Mpc_ArepoPDF). The default settings are also applied to a smaller sample of 240 galaxies in the SIMBA-25 box as a convergence test (25Mpc_ArepoPDF). Finally, we also investigate the resulting line emission when not including the additional sub-grid attenuation function as described in Section 2.4.1 and otherwise adopted in the default run (100Mpc_ArepoPDF_NO_EXT).
### 3.3. Observed galaxy sample for comparison

We will be comparing the different simulation runs with a broad selection of nearby observed galaxies. Since the samples of simulated galaxies were selected to span a wide range in stellar mass, SFR, and gas mass, they were not tailored to match any specific observed sample. We will be comparing the range in simulated and observed line luminosities as a function of SFR, looking for agreements on the order of magnitude and deferring a more careful comparison with observations to a future study. The sample of observed galaxies comprises all nearby galaxies observed with Herschel or the Infrared Space Observatory that we could find in the literature for which a good agreement is reached, but it completely overlaps with the observed line luminosity–SFR relation. The different sGAME runs listed in Table 3 can now be compared for each of the eight emission lines considered here, with the fine-structure lines sorted in order of increasing critical density (Table 1). Due to the mixed sample of observed galaxies that we compare to, we define a “good agreement” here as when the quartile spread around the observed line luminosity–SFR relation.

For run 100Mpc_M10, the resulting deviations from observations are shown with orange bars. Surprisingly, this simple assumption does a very good job for the ionized species of \([\text{N}\,\text{II}]\,205, \ [\text{O}\,\text{II}]\,88\) and \([\text{C}\,\text{II}]\), for which a good agreement is reached, but it completely underestimates CO emission. The CO(1-0), (2-1) and (3-2) lines fall below the observed line-SFR relation by median deviations of 3.4, 3.9 and 3.5 dex, respectively. The underestimation of the molecular lines is not surprising, given that the density PDF does not extend significantly beyond densities > 10^2 cm^{-3} where molecules form (see Fig. 7).

| Run name             | Description                                                                 |
|----------------------|-----------------------------------------------------------------------------|
| 100Mpc_M10           | Adopting one lognormal with Mach number 10 with a forcing parameter 1/3 for the sub-grid density profile (see Section 2.3). |
| 100Mpc_SIGAMEv2      | Comparison run with sGAME v2 applied to the SIMBA-100 sample.               |
| 100Mpc_arepoPDF      | Adopting density PDFs with a power-law tail as parameterized for a higher-resolution AREPO-M51 simulation (see Section 2.3). This is our “default run”. |
| 25Mpc_arepoPDF       | Same as “100Mpc_arepoPDF” but for the SIMBA-25 simulation volume (see Section 3.1). |
| 100Mpc_arepoPDF_no_ext | Same as “100Mpc_arepoPDF” but without the additional extinction function described in Section 2.4.1. |
With run $100\text{Mpc\_SIGAMEv2}$ (purple bars), we test how well the previous $\text{SIGAME}$ framework, which has so far only been applied at $z \sim 2$ and above, works for the $\text{SI MBA-100}$ $z = 0$ sample. While this version of the code gives a good agreement with observations for $[\text{C\ II}]$, $[\text{O\ I}]63$, CO(1-0) and CO(3-2), it significantly underestimates the $[\text{N\ II}]$ and $[\text{O\ III}]88$ lines with median deviations larger than 1 dex. For all lines except $[\text{O\ I}]63$, this version also produces outliers with extremely low line luminosities, as shown with open circles (and indeed, the plot does not extend to show all outliers). We attribute this disagreement to the simplified gas fragmentation scheme used in $\text{SIGAME}$ v2 in which gas particles were split into either GMCs following a locally observed mass spectrum or diffuse gas, with no intermediate ISM phase and no sanity checks on the density PDF.

The default run of the current version of $\text{SIGAME}$, $100\text{Mpc\_AREPOPDF}$ (green bars) comes closest to all line luminosities simultaneously, with the fewest outliers. In total, six out of the eight lines considered here are in good agreement with the observed relations, while the lines of $[\text{O\ I}]63$ and CO(3-2) line luminosities are overestimated by median deviations of 1.3 and 1.0 dex, respectively, compared to the observations. We do not consider the overestimation of CO(3-2) an outstanding problem due to the lack of observations compiled here (our observed comparison sample comprises 21 galaxies).

The test run without additional extinction, $100\text{Mpc\_AREPOPDF\_NO\_EXT}$ (brown bars), looks very similar to the default run in Fig. 9 with the most noticeable difference being an increased $[\text{O\ I}]63$ line prediction that falls above the observed luminosities by a median deviation of 1.9 dex. In our default run, with the user-defined attenuation function described in Section 2.4.1, the overestimation of $[\text{O\ I}]63$ is brought down by about 0.5 dex to 1.3 dex above the observed $[\text{O\ I}]63$ SFR relation, and the tail of low CO luminosities is reduced in length by several dex. This suggests that the inclusion of additional attenuation is necessary in order for enough O I and CO to form. An effect on the $[\text{N\ II}]$ and $[\text{O\ III}]88$ lines could also be expected since these lines originate in dense H II regions. Although the current version of $\text{SIGAME}$ does not explicitly model H II regions...
(see the discussion in Section 4.3), the additional attenuation at densities above $10^2 \text{cm}^{-3}$ should also affect these lines, but this is not clear from the distributions in Fig. 9 alone. In order to investigate the effect of additional attenuation, Fig. 10 compares the default run (100MPC\_AREPOPDF) to that without additional attenuation (100MPC\_AREPOPDF\_NO\_EXT) as a function of galaxy properties $M_\star$, $M_{\text{gas}}$, SFR, and $(Z)_{\text{SFR}}$. Only the CO and [O I]63 line luminosities are consistently higher and lower, respectively, in the default run, in agreement with Fig. 9. The deviations in the [N II], [O III]88 and [C II] line luminosities are negligible at the lower end of $M_\star$, $M_{\text{gas}}$, SFR and $(Z)_{\text{SFR}}$, but tend toward negative values at the higher end. In particular, the [N II] and [O III]88 lines are more strongly affected by the additional attenuation for high values of SFR and $(Z)_{\text{SFR}}$ (rightmost two panels). This behavior can be explained by considering what happens in the one-zone CLOUDY models of which our look-up table consists. At higher metallicities, increasing self-shielding of nitrogen and oxygen results in more singly ionized nitrogen and doubly ionized oxygen relative to higher ionization states since the one-zone CLOUDY models include self-shielding. This in turn results in higher [N II] and [O III]88 luminosities with increasing metallicity for a given one-zone CLOUDY model and hence a strong dependence on metallicity in run 100MPC\_AREPOPDF\_NO\_EXT. However, once additional attenuation is added at densities above $100 \text{cm}^{-3}$, the luminosity of those one-zone models is negligible as there is no ionizing radiation to ionize nitrogen and oxygen. The difference between the two runs is therefore more pronounced at high metallicity, where models with densities above $100 \text{cm}^{-3}$ have had their [N II] and [O III]88 luminosities dramatically reduced. Since there is a weak correlation between SFR and $(Z)_{\text{SFR}}$ in our sample, the same can be said for the evolution with SFR seen in Fig. 10.

Finally, the test run with default settings at higher mass resolution, 25MPC\_AREPOPDF (blue bars), shows quartile ranges that overlap with those of the SIMBA-100 sample, indicating that the SIGAME results do not depend significantly on mass resolution in the underlying simulation. However, this analysis alone does not reveal any bias due to the different galaxy properties of the two samples. In Fig. 14 in Appendix D we investigate in more depth how well the two simulation runs agree with one another for a range of physical galaxy properties, finding that for similar galaxies, the luminosities of [N II]122, [N II]205, [O III]88, [C II] and [O I]63 tend to be overestimated by up to $\sim 0.5$–1.5 dex in SIMBA-25 compared to SIMBA-100, in particular at high SFR and $(Z)_{\text{SFR}}$. It is interesting to note that 100MPC\_AREPOPDF\_NO\_EXT behaves more similarly to 25MPC\_AREPOPDF than to 100MPC\_AREPOPDF, and it is hard to say whether this is a resolution issue or due to the attenuation function present in the latter two runs.

4. DISCUSSION

4.1. Comparison with previous models

We can compare our [C II]–SFR relation with that found through similar techniques and hence better understand the decisive differences between the models. Figure 11 shows the [C II]–SFR relations found by SIGAME for the SIMBA-100 galaxies with the 100MPC\_AREPOPDF and run (green contour lines) together with the relations derived by Popping et al. (2019) and Ramos Padilla et al. (2021). From the 100MPC\_AREPOPDF run, we also show the distribution of only main-sequence (MS) galaxies, chosen to be between the 16th and 84th percentile of the Salim et al. (2018) relation (purple dashed contour lines).
The distribution of sIGAME simulated galaxies generally matches that of the observed galaxies well, but fails to reproduce the some of the galaxies of lower [C II] luminosity and the nondetections of Brauher et al. (2008). Selecting only MS galaxies does not change this picture significantly. Our simulated galaxies lie in above the simulated sample of Popping et al. (2019), but in apparent extension of the samples of Ramos Padilla et al. (2021), made with cosmological simulations from the Evolution and Assembly of Galaxies and their Environments (EAGLE) project (Crain et al. 2015; Schaye et al. 2015). In the latter study, GMCs are created in post-processing following Olsen et al. (2015) and Cloudy is used to derive line intensities as in newer versions of sIGAME. One interesting avenue of further study would be to apply sIGAME to EAGLE, to fully understand how intrinsic differences between EAGLE and SIMBA affect this comparison.

Another interesting comparison can be made to the CO line modeling of Vallini et al. (2018) (hereafter V18) in which the sub-grid density PDF was determined using the Mach number of the underlying simulation together with a time-dependent evolution of the high-density power law tail. V18 find good agreement with this comparison. Another interesting comparison can be made to the CO line modeling of Vallini et al. (2018) (hereafter V18) in which the sub-grid density PDF was determined using the Mach number of the underlying simulation together with a time-dependent evolution of the high-density power law tail. V18 find good agreement with this comparison.

Figure 11. Comparison of the sIGAME v3 [C II]–SFR relation (100Mpc_AREPOPDF; green; MS-only galaxies: purple dashed contour lines) with other recent modeling efforts: a multiphase model of the ISM used as a postprocessing step for the EAGLE cosmological hydrodynamical simulations (cyan, orange, and dark blue contour lines; Ramos Padilla et al. 2021), and the z = 0 [C II]–SFR relation found by Popping et al. (2019) using semianalytical models (black line), with a 1σ shaded region. Observations of nearby galaxies are shown with gray symbols (Brauher et al. 2008; Díaz-Santos et al. 2013; Cormier et al. 2015; Kamenetzky et al. 2016; Accurso et al. 2017) and the [C II]–SFR relations for local starburst and dwarf galaxies by De Looze et al. (2014) are shown with gray dotted and dashed lines, respectively.

4.2. Choice of simulation for the fragmentation task

We have only shown results for the present framework using one type of simulation, namely the AREPO suite of M51 realizations. We also examined an AREPO simula-
portant, although a better test would be to compare with an entirely different galaxy simulation (not just a special region like the CMZ).

Another caveat associated with the approximations used for the AREPO-M51 simulations is a tendency for the clouds to be too long-lived, which might in turn yield too little SFR for a given surface density. Of relevance to SIGAME, this could mean that we are overestimating the number of clouds (i.e. dense gas mass fraction in the PDF) for a given SFR volume density. However, choosing a completely different galaxy simulation technique (e.g. models run with adaptive mesh refinement codes such as RAMSES, ENZO, or ATHENA—Teyssier 2002; Bryan et al. 2014; Kim & Ostriker 2017) might return different PDFs, the effect of which we have not studied. Instead, we have focused on making the current version of SIGAME flexible and publicly available so that the user can include any high-resolution simulation for the gas fragmentation if they so desire.

4.3. Small-scale radiation field structure

As discussed in the previous section, this version of SIGAME fragments the gas density on scales smaller than the Skirt cell sizes (typically larger than \(\sim 15 \) pc), thereby allowing for clumps of higher densities on scales not resolved by the parent simulation. In a similar manner, we could also expect the radiation field to be fragmented such that the mass-weighted FUV flux distribution on parsec scales can differ substantially from the overall cell mean flux value and allow for parsec-size features such as H II regions or shielded, dense, molecular cores. Judging from the overall agreement between simulated and observed lines, we speculate that most of the FIR lines considered here arise from structures of larger extent where parsec resolution in radiation is not necessary, with the exception of [O I]63, which is overestimated. The continued overestimation of the [O I]63 and CO(3-2) line emission by our default run (see Fig. 9) suggests that a more careful treatment of the sub-grid attenuation and/or other features remains missing, however. A proper treatment of the flux distribution on these scales would require considerations about the properties of natal clouds around young stars, as demonstrated with the one-dimensional stellar feedback model WARPFIELD (Rahner et al. 2017). In addition, [C II] and [O III]88 remain slightly overestimated, both of which originate mainly in the atomic ISM phase in our model, hinting at an overestimation of atomic gas mass versus ionized gas mass in our gas fragmentation scheme.

4.3.1. Missing treatment of active galactic nuclei

While the coevolution of AGNs and their host galaxies is simulated in SIMBA, the current version of SIGAME does not include any effects of AGN presence, such as additional heating and radiation. The additional X-ray heating has been shown to increase excitation of high-J CO lines at high redshifts (Vallini et al. 2019).

4.4. Missing shock-heating of the gas

In starburst galaxies and mergers, shocks are expected to act as an additional heating source in the ISM. Although the next version of CLOUDY may include a treatment for shock-heated gas the current version of CLOUDY iterates to find a thermal and ionization equilibrium, thereby ignoring any shocked state of the gas that might be present in the simulation. One way to treat shock-heated gas, would be to set up a separate grid of models, following the technique used for MAP-PINGS III (Allen et al. 2008). Turbulence (2–10 km s\(^{-1}\)) in velocity dispersion) and/or density-dependent magnetic fields are also believed to play a role in setting the [O I]63 emission, through their effect on line width, shielding and pumping, and the chemical and thermal state of the gas (Canning et al. 2016). However, testing the effect of these would require CLOUDY models of more than one zone where optical depth is taken into account.

5. CONCLUSIONS

This paper introduces an improved algorithm for estimating FIR line emission from large-volume cosmological galaxy simulations using coarse numerical resolution. We postprocess such simulations using a sub-grid model that estimates the distribution of dense gas up to densities of \(\sim 10^7\) cm\(^{-3}\). This fragmentation scheme results in gas at lower densities being compressed to higher densities, and hence affects emission lines tracing all ISM phases. We test the scheme on eight low-to-medium-density ISM tracers.

The density distribution on sub-grid scales is modeled by sorting and parameterizing resolved regions in higher-resolution simulations and interpolating on the parameterized functions to set the density distribution for the cosmological simulations. This statistical approach avoids any assumption about the size and shape of molecular clouds, the turbulence within those clouds, or the existence of pressure equilibrium between the dense and more diffuse ISM phases. As a demonstration of this scheme, we use data with subparsec resolution from a model of M51 with AREPO (Tress et al. 2020). Density PDFs are sampled in 200 pc regions and binned in terms of the volume-averaged hydrogen and SFR density of each region. The resulting mean PDFs are parameterized and used to generate PDFs by interpolation for each resolution element of the cosmological simulation to generate gas densities \(\sim 10^2\)–\(10^7\) cm\(^{-3}\).
otherwise not present in the cosmological simulation results. As a future extension, this approach could also be used to develop a new SFR prescription for cosmological simulations.

The local radiation field strength is determined with the radiative transfer code Skirt, which calculates the local dust-attenuated stellar spectrum. The SWIFT-simIO package is used to map gas properties from the cosmological simulation output to the cell structure from Skirt. Additional attenuation by gas is implemented through a set of Cloudy models, by matching the transmitted spectrum in the OIR-to-FUV of a certain column density of gas to the dust-attenuated spectrum of Skirt for each gas cell. Line emission and chemical information are derived from an extensive grid of 129,600 Cloudy one-zone models, sampled according to the local density PDF to create a library totalling 259,200 models of different combinations of $n_H$, ($n_{\text{SFR}}$)$_V$, $N_H$, $F_{\text{FUV}}$, $Z$ and DTM ratio. Finally, to compensate for lack of resolution in the cosmological simulations used here, we add attenuation on sub-grid scales with a simple function that can be modified by the user to work on other simulation types. In this case, we add attenuation for Cloudy grid models with $n_H > 10^2$ cm$^{-3}$.

We test the method on the Simba cosmological simulations by extracting galaxies that span a wide range in stellar mass, SFR, and $Z$. As a rough validation of the method, results are compared to observed relations between line luminosity and SFR for a diverse sample of nearby galaxies and eight different emission lines. To test how well the method converges for different mass resolutions, we apply Simba to the Simba-100 and 25 Mpc volumes, the latter of which has roughly eight times higher mass resolution for the gas particles. We also compare with results using the previous version of Simba (v2) and results when not including the user-defined attenuation function. Finally, the method is also checked against the default option of adopting a lognormal density profile drawn from Mach 10 isothermal turbulence for the sub-grid density profile, although we expect this method to fare poorly in the case of cosmological simulations. These tests leave us with the following conclusions.

- The novel method presented here of using a high-resolution simulation and a new analytic PDF approach for the gas fragmentation results in emission lines that are in good agreement (i.e. the quartile values overlap with the $2\sigma$ spread around the observed line–SFR relation) for all but the [O I]63 and CO(3-2) lines that are overestimated by on average 1.3, 1.0 dex, respectively.

- We find that the resulting line emission of [O I]63 in particular is highly dependent on the user-defined attenuation function, without which the overestimation of the [O I]63 luminosities is about 0.5 dex higher still. This underlines the need for a more careful treatment of the radiation on sub-grid scales ($< 200$ pc), where denser regions should produce additional attenuation of the interstellar radiation field than what is included in this framework by default.

- We find a good agreement with observations of nearby galaxies and other models in terms of [C II]-SFR relation, although our default model cannot reproduce the non-detections of [C II].

- Comparing line luminosities of galaxies in the Simba-100 and Simba-25 samples, we find that the latter returns higher luminosities by up to $\sim 0.5–1.5$ dex, in particular at high SFR and SFR-weighted $Z$.

- Comparing with the previous version of Simba (v2), we find that this method significantly underestimates the [N II] and [O III]88 lines with median deviations larger than 1 dex, most likely due to a simplified ISM structure.

- The standard method in the literature of adopting the density PDF of Mach 10 isothermal turbulence for fragmenting gas on sub-grid scales results in FIR fine-structure line emission that agrees well with observations for lines originating mainly in the ionized ISM, but drastically underestimates lines from the neutral and molecular regions. For example, the CO(1-0), (2-1) and (3-2) rotational lines fall below the observed line-SFR relation by median deviations of 3.4, 3.9 and 3.5 dex, respectively.

We have presented Simba v3 which is a flexible framework that can be adapted to any cosmological or galaxy simulation, and now has the option to further fragment the gas on sub-grid scales using a high-resolution simulation of choice. This tool may be useful for the interpretation of current data from e.g. ALMA, NOEMA and SOFIA as well as from future space and balloon missions such as JWST, GUSTO, and ASTHROS.
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REFERENCES

Accurso, G., Saintonge, A., Catinella, B., et al. 2017, MNRAS, 470, 4750, doi: 10.1093/mnras/stx1556
Allen, M. G., Groves, B. A., Dopita, M. A., Sutherland, R. S., & Kewley, L. J. 2008, ApJS, 178, 20, doi: 10.1086/589652
Alves, F. O., Cleeves, L. I., Girart, J. M., et al. 2020, ApJL, 904, L6, doi: 10.3847/2041-8213/abc550
Alves, J., Lombardi, M., & Lada, C. J. 2017, A&A, 606, L2, doi: 10.1051/0004-6361/201731436
Appleby, S., Davé, R., Kraljic, K., Anglés-Alcázar, D., & Narayanan, D. 2020, MNRAS, 494, 6053, doi: 10.1093/mnras/staa1169
Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, A&A, 558, A33, doi: 10.1051/0004-6361/201322068
Bigiel, F., Leroy, A., Walter, F., et al. 2008, AJ, 136, 2846, doi: 10.1088/0004-6256/136/6/2846
Borrow, J., & Borrisov, A. 2020, The Journal of Open Source Software, 5, 2430, doi: 10.21105/joss.02430
Brauher, J. R., Dale, D. A., & Helou, G. 2008, ApJS, 178, 280, doi: 10.1086/590249
Bryan, G. L., Norman, M. L., O'Shea, B. W., et al. 2014, ApJS, 211, 19, doi: 10.1088/0067-0049/211/2/19
Burkhart, B. 2018, ApJ, 863, 118, doi: 10.3847/1538-4353/aad062
Burkhart, B., Collins, D. C., & Lazarian, A. 2015, ApJ, 808, 48, doi: 10.1088/0004-637X/808/1/48
Burkhart, B., & Mocz, P. 2019, ApJ, 879, 129, doi: 10.3847/1538-4357/ab25ed
Burkhart, B., Stalpes, K., & Collins, D. C. 2017, ApJL, 834, L1, doi: 10.3847/2041-8213/834/1/L1
Calzetti, D., Wu, S. Y., Hong, S., et al. 2010, ApJ, 714, 1256, doi: 10.1088/0004-637X/714/2/1256
Camps, P., & Baes, M. 2020, Astronomy and Computing, 31, 100381, doi: 10.1016/j.ascom.2020.100381
Canning, R. E. A., Ferland, G. J., Fabian, A. C., et al. 2016, MNRAS, 455, 3042, doi: 10.1093/mnras/stv2390
Chabrier, G. 2003, PASP, 115, 763, doi: 10.1086/376392
Chen, H. H.-H., Burkhart, B., Goodman, A., & Collins, D. C. 2018, The Astrophysical Journal, 859, 162, doi: 10.3847/1538-4357/aabaf6
Chevance, M., Kruisjens, J. M. D., Vazquez-Semadeni, E., et al. 2020, SSRv, 216, 50, doi: 10.1007/s12121-020-00674-x
Collins, D. C., Kritsuk, A. G., Padoan, P., et al. 2012, ApJ, 750, 13, doi: 10.1088/0004-637X/750/1/13
Colombo, D., Hughes, A., Schinnerer, E., et al. 2014, ApJ, 784, 3, doi: 10.1088/0004-637X/784/1/3
Conroy, C., & Gunn, J. E. 2010, ApJ, 712, 833, doi: 10.1088/0004-637X/712/2/833
Conroy, C., Gunn, J. E., & White, M. 2009, ApJ, 699, 486, doi: 10.1088/0004-637X/699/1/486
Cornier, D., Madden, S. C., Lebouteiller, V., et al. 2015, A&A, 578, A53, doi: 10.1051/0004-6361/201425207
Cowie, L. L., & Songaila, A. 1986, ARAA, 24, 499, doi: 10.1146/annurev.aa.24.090186.002435
Craín, R. A., Schaye, J., Bower, R. G., et al. 2015, MNRAS, 450, 1937, doi: 10.1093/mnras/sts725
Davé, R., Anglés-Alcázar, D., Narayanan, D., et al. 2019, MNRAS, 486, 2827, doi: 10.1093/mnras/stz937
Davé, R., Thompson, R., & Hopkins, P. F. 2016, MNRAS, 462, 3265, doi: 10.1093/mnras/stw1862
De Loore, I., Cormier, D., Lebouteiller, V., et al. 2014, A&A, 568, A62, doi: 10.1051/0004-6361/201322489
Díaz-Santos, T., Armus, L., Charmandaris, V., et al. 2013, ApJ, 774, 68, doi: 10.1088/0004-637X/774/1/68
—. 2017, ApJ, 846, 32, doi: 10.3847/1538-4357/aa81d7
Eldridge, J. J., Stanway, E. R., Xiao, L., et al. 2017, PASA, 34, e058, doi: 10.1017/pasa.2017.51
Farrah, D., Lebouteiller, V., Spoon, H. W. W., et al. 2013, ApJ, 776, 38, doi: 10.1088/0004-637X/776/1/38
Federrath, C., Klessen, R. S., & Schmidt, W. 2008, ApJ, 688, L79, doi: 10.1086/595280
Ferland, G. J., Chatzikos, M., Guzmán, F., et al. 2017, RMxAA, 53, 385. https://arxiv.org/abs/1705.10877
Foreman-Mackey, D., Sick, J., & Johnson, B. 2014, python-fsps: Python bindings to FSPS (v0.1.1), v0.1.1, Zenodo, doi: 10.5281/zenodo.12157
Girichidis, P., Konstandin, L., Whitworth, A. P., & Klessen, R. S. 2014, ApJ, 781, 91, doi: 10.1088/0004-637X/781/2/91
Gnedin, N. Y., Kravtsov, A. V., & Chen, H.-W. 2008, ApJ, 672, 765, doi: 10.1086/524007
Gnedin, N. Y., Tassis, K., & Kravtsov, A. V. 2009, ApJ, 697, 55, doi: 10.1088/0004-637X/679/1/55
Goldreich, P., & Kwan, J. 1974, ApJ, 189, 441, doi: 10.1086/152821
Goldsmith, P. F., Langer, W. D., Pineda, J. L., & Velusamy, T. 2012, ApJS, 203, 13, doi: 10.1088/0067-0049/203/1/13
Habing, H. J. 1968, BAN, 19, 421
Harris, C. R., Millman, J., van der Walt, S. J., et al. 2020, Nature, doi: 10.1038/s41586-020-2649-2
Hennebelle, P., & Inutsuka, S.-i. 2019, Frontiers in Astronomy and Space Sciences, 6, 5, doi: 10.3389/fspas.2019.00005
APPENDIX

A. PROPERTIES OF SIMBA-100 MODEL GALAXY SAMPLE

Table 4 lists the physical properties of the SIMBA-100 galaxy sample while Table 5 lists their line luminosities, including a few \( L_{[O\text{I}]145} \), \( L_{[C\text{I}]610} \) and \( L_{[C\text{I}]371} \) not used in the validation of the method.

Table 4. Physical Properties of the Sample of 400 SIMBA-100 Galaxies Used in This Work.

| Galaxy Index | \( \log M_\star \) \( (10^9 M_\odot) \) | \( \log M_{\text{gas}} \) \( (10^9 M_\odot) \) | SFR \( (M_\odot \text{ yr}^{-1}) \) | \( \langle Z \rangle_{\text{SFR}} \) \( (Z_\odot) \) | \( \langle Z \rangle_{\text{new}} \) \( (Z_\odot) \) |
|-------------|---------------------------------|---------------------------------|----------------|----------------|----------------|
| 0           | 0.4148                          | 6.6530                          | 0.35           | 0.16           | 0.02           |
| 1           | 0.4594                          | 7.6858                          | 0.37           | 0.10           | 0.03           |
| 2           | 0.4923                          | 6.1911                          | 0.18           | 0.12           | 0.05           |
| 3           | 0.5001                          | 9.5347                          | 0.18           | 0.13           | 0.02           |
| 4           | 0.5318                          | 8.6812                          | 0.38           | 0.16           | 0.04           |
| 5           | 0.5342                          | 6.3430                          | 0.35           | 0.14           | 0.05           |
| 6           | 0.5406                          | 10.0238                         | 0.54           | 0.15           | 0.04           |
| 7           | 0.5561                          | 7.0146                          | 0.17           | 0.15           | 0.03           |
| 8           | 0.5646                          | 6.3235                          | 0.52           | 0.11           | 0.02           |
| 9           | 0.5948                          | 5.8621                          | 0.69           | 0.15           | 0.06           |

Note—\( \langle Z \rangle_{\text{new}} \) stands for mass-weighted gas-phase metallicity.
This table is available online in its entirety in machine-readable format.
Table 5. Line Luminosities for the Sample of 400 SIMBA-100 Galaxies Used in This Work.

| Galaxy index | \(L_{[\text{CI}]158}\) | \(L_{[\text{CI}]610}\) | \(L_{[\text{NII}]371}\) | \(L_{[\text{NII}]122}\) | \(L_{[\text{OII}]145}\) | \(L_{[\text{OIII}]88}\) | \(L_{\text{CO}(1-0)}\) | \(L_{\text{CO}(2-1)}\) | \(L_{\text{CO}(3-2)}\) |
|--------------|----------------|----------------|----------------|----------------|----------------|----------------|---------------|---------------|---------------|
| 0            | 1.32e+07       | 4.38e+04       | 1.45e+05       | 2.73e+06       | 5.25e+05       | 3.39e+05       | 8.33e+06      | 4.10e+06      | 2.64e+02      | 5.82e+03      | 2.81e+04      |
| 1            | 4.53e+07       | 2.33e+04       | 1.30e+05       | 1.38e+07       | 3.28e+07       | 1.35e+06       | 4.54e+07      | 3.65e+07      | 1.12e+02      | 3.15e+03      | 1.98e+04      |
| 2            | 2.13e+07       | 5.74e+04       | 1.70e+05       | 4.22e+06       | 8.29e+06       | 1.16e+06       | 3.51e+07      | 5.67e+06      | 8.64e+02      | 2.20e+04      | 1.21e+05      |
| 3            | 2.16e+07       | 5.54e+04       | 2.22e+05       | 5.43e+06       | 9.33e+06       | 5.15e+05       | 1.20e+07      | 2.95e+06      | 4.58e+02      | 1.13e+04      | 6.14e+04      |
| 4            | 6.18e+07       | 3.01e+04       | 1.61e+05       | 1.83e+07       | 4.49e+07       | 2.54e+06       | 9.40e+07      | 1.16e+08      | 1.58e+02      | 4.47e+03      | 2.84e+04      |
| 5            | 6.26e+07       | 3.20e+04       | 1.70e+05       | 1.85e+07       | 4.28e+07       | 1.96e+06       | 5.99e+07      | 4.45e+07      | 2.14e+02      | 6.08e+03      | 3.87e+04      |
| 6            | 6.42e+07       | 5.20e+04       | 2.73e+05       | 1.93e+07       | 4.17e+07       | 1.79e+06       | 4.98e+07      | 3.76e+07      | 3.74e+02      | 9.91e+03      | 5.76e+04      |
| 7            | 8.17e+06       | 3.89e+04       | 1.02e+05       | 1.38e+06       | 2.19e+06       | 2.94e+05       | 8.91e+06      | 8.28e+05      | 4.73e+02      | 1.08e+04      | 5.43e+04      |
| 8            | 2.28e+07       | 3.07e+04       | 1.28e+05       | 4.43e+06       | 8.29e+06       | 7.76e+05       | 2.17e+07      | 3.89e+06      | 1.73e+02      | 4.68e+03      | 2.81e+04      |
| 9            | 6.87e+07       | 3.20e+04       | 1.71e+05       | 1.82e+07       | 4.33e+07       | 3.87e+06       | 1.41e+08      | 1.10e+08      | 2.60e+02      | 7.38e+03      | 4.70e+04      |

Note—This table is available online in its entirety in machine-readable format.
B. CONVERGENCE TESTS WITH SKIRT

SKIRT uses a fixed set of photon packets when iterating for a solution to the radiative transfer problem. We tested SKIRT with different photon packet numbers for the galaxy with the largest stellar mass in SIMBA-100, corresponding to 39,733 stellar particles. The resulting total FUV luminosity and FUV flux distribution can be seen in Figure 12 for photon packet sizes of $10^6$, $10^7$, $10^8$ and $10^9$, corresponding to $2.5 \times 10^1$, $2.5 \times 10^2$, $2.5 \times 10^3$ and $2.5 \times 10^4$ to photon packets per source. There is only a negligible change in FUV luminosity of 1.86% compared to using the lowest number of photon packets, but when looking at the flux distribution it becomes clear that at least $10^8$ packets are necessary for a stable result, whereas increasing the number to $10^9$ has little effect. We therefore settled on $10^8$ photon packets.

![Figure 12](image)

**Figure 12.** Convergence tests of the SKIRT FUV output for different total numbers of photon packets used in the calculation.
C. DISTRIBUTION OF CELL PHYSICAL PARAMETERS

Figure 13 shows the volume-averaged gas and SFR densities for all cells in all galaxies of our sample. The grid point values in \( \langle n_H \rangle_V \) and \( \langle n_{\text{SFR}} \rangle_V \) used to sample the CLOUDY grid are also shown in Figure 13. The cells in the SIMBA galaxies have a larger spread in \( \langle n_{\text{SFR}} \rangle_V \) and go to lower \( \langle n_H \rangle_V \) than the chosen grid points, reflecting a larger parameter space than what is found in AREPO-M51. However, we do not expect this to be a problem since the effect of \( \langle n_{\text{SFR}} \rangle_V \) on the density PDF is less than that of \( \langle n_H \rangle_V \) as seen in Figure 3 and the regions of low \( \langle n_H \rangle_V \) are treated separately.

Figure 13. Contour plot showing the cell distribution in density and SFR volume density for all 400 sample galaxies. The horizontal dashed lines indicate the center of the \( \langle n_{\text{SFR}} \rangle_V \) bins shown in Figure 3, while the vertical dashed lines correspond to the densities used to sample the SIMBA gas densities in Section 2.4. Cells with \( \langle n_{\text{SFR}} \rangle_V = 0 \text{M}_\odot \text{yr}^{-1} \text{kpc}^{-3} \) are set to \( \langle n_{\text{SFR}} \rangle_V = 10^{-5} \text{M}_\odot \text{yr}^{-1} \text{kpc}^{-3} \) in order to show their density distribution in the plot.
D. COMPARISON OF SIMILAR GALAXIES IN SIMBA-100 AND SIMBA-25

In order to make a fair comparison of the line emission calculated by SIGAME for the different SIMBA volumes used here, we have selected a handful of galaxies in both SIMBA-100 and SIMBA-25 that have similar global properties in terms of $M_*$, $M_{\text{gas}}$, SFR, and $\langle Z \rangle_{\text{SFR}}$. We identify “galaxy pairs” by searching for the smallest distance in the 4D parameter space spanned by the $M_*$, $M_{\text{gas}}$, SFR, and $\langle Z \rangle_{\text{SFR}}$ values, all in log units and normalized to lie in the range from 0 to 1. The result can be seen in Figure 14 in which the luminosity in SIMBA-100 is subtracted from the luminosity in SIMBA-25 for each galaxy pair to give a deviation in luminosity, as function of $M_*$, $M_{\text{gas}}$, SFR and $\langle Z \rangle_{\text{SFR}}$. The colored lines show the closest pair for the parameter of that panel while the shaded regions show the range in luminosities from the 25th to 75th percentile for all galaxy pairs in that bin. A dashed horizontal line shows a deviation of 0, signalling that the two galaxies have equal line luminosity. The luminosities of [N II]122, [N II]205, [O III]88, [C II] and [O I]63 tend to be overestimated by up to $\sim 0.5$–$1.5$ dex in SIMBA-25 compared to SIMBA-100, in particular at higher values of SFR and $\langle Z \rangle_{\text{SFR}}$. We attribute the larger deviations at low values of $M_*$ and $M_{\text{gas}}$ to the lower mass resolution in SIMBA-100 compared to SIMBA-25. To illustrate the lack in resolution, a vertical dashed line indicates the minimum gas mass in our SIMBA-100 sample with at least 500 gas particles, which is $5.6 \times 10^9 \, M_\odot$. The mass resolution of SIMBA-25 is a factor of 8 higher, with the initial gas particle mass in SIMBA-100 being $1.82 \times 10^7 \, M_\odot$, compared to $2.28 \times 10^6 \, M_\odot$ in SIMBA-25. Our SIMBA-25 selection contains galaxies with gas masses down to $7.3 \times 10^8 \, M_\odot$, with the constraint that they contain at least 500 gas particles.

Figure 14. Deviation in line luminosity between galaxies of similar $M_*$, $M_{\text{gas}}$, SFR and $\langle Z \rangle_{\text{SFR}}$ in SIMBA-100 vs SIMBA-25 as a function of those global properties. Only the eight emission lines considered in this paper are considered, shown here with different colors. Shaded regions show the range in luminosities from the 25th to 75th percentile for all galaxy pairs in that bin.
E. IMPACT OF DIFFERENT DENSITY PDFS ON LINE LUMINOSITY DISTRIBUTION

In Fig. 15 we explore the origin of line emission with respect to hydrogen density for the different sub-grid density PDF prescriptions adopted in this paper for each of the eight emission lines investigated here. As shown in Fig. 7 the resulting sub-grid densities are generally no larger than around $10 \text{ cm}^{-3}$ when restricting the density PDF shape to that of a lognormal of Mach number 10 and $b = 1/3$ centered at the gas density from the simulation for each cell. In Fig. 15 this means all line luminosity is restricted to come from densities below around $10 \text{ cm}^{-3}$, as the orange dotted lines show. In Section 4.2 we describe the AREPO-CMZ run, which was used as an alternative simulation to generate tables of density PDFs. In particular, the PDF tables generated with AREPO-CMZ yield more mass at higher densities in the regime of low average cell density ($\log n_H < 0$). This can also be seen in Fig. 15, where the line luminosity distributions with AREPO-CMZ (blue, dashed) are skewed toward higher densities than the default result using AREPO-M51 (cyan, solid). Due to the differences between the M51 case and the comparatively extreme CMZ environment and hence between the two simulations as described in Section 4.2, these significant changes in line luminosity distribution are indeed expected. Finally, the run using the AREPO-M51 simulation but no attenuation at high densities (brown, dotted–dashed), as otherwise done following the description in Section 2.4, returns the same density distribution as the default run, but the missing extinction results in overall lower or higher luminosities, depending on the line considered. Specifically, for the higher ionization lines of [N II]122, [N II]205 and [O III]88 the line luminosities are higher without the extinction in the FUV, while the CO line luminosities are lower, since the missing extinction means that less CO is able to form. A note of caution when interpreting Fig. 15 is that the density on the x-axis is a mass-weighted density of all the one-zone CLOUDY models used to calculate the line luminosity of that cell. It is not weighted by where the line emission is actually coming from (luminosity-weighted).
Figure 15. Line luminosity per cell integrated over different hydrogen density bins in the SIMBA-25 galaxy shown in the top panels of Figs. 6 and 8. Different line styles refer to different methods for deriving the sub-grid density PDF: with the default AREPO-M51 simulation (cyan, solid), with the AREPO-CMZ simulation (blue, dashed), with the AREPO-M51 simulation and no attenuation at high densities (brown, dotted-dashed), and with a fixed lognormal shape corresponding to a Mach number of 10 and $b = 1/3$, see eq. 4 (orange, dotted).