Hierarchical self-entangled carbon nanotube tube networks

Fabian Schütt1, Stefano Signetti2, Helge Krüger1, Sarah Röder1, Daria Smazna1, Sören Kaps1, Stanislav N. Gorb3, Yogendra Kumar Mishra1, Nicola M. Pugno2,4,5 & Rainer Adelung1

Three-dimensional (3D) assemblies based on carbon nanomaterials still lag behind their individual one-dimensional building blocks in terms of mechanical and electrical properties. Here we demonstrate a simple strategy for the fabrication of an open porous 3D self-organized double-hierarchical carbon nanotube tube structure with properties advantageous to those existing so far. Even though no additional crosslinking exists between the individual nanotubes, a high reinforcement effect in compression and tensile characteristics is achieved by the formation of self-entangled carbon nanotube (CNT) networks in all three dimensions, employing the CNTs in their high tensile properties. Additionally, the tubular structure causes a self-enhancing effect in conductivity when employed in a 3D stretchable conductor, together with a high conductivity at low CNT concentrations. This strategy allows for an easy combination of different kinds of low-dimensional nanomaterials in a tube-shaped 3D structure, enabling the fabrication of multifunctional inorganic-carbon-polymer hybrid 3D materials.

1Functional Nanomaterials, Institute for Materials Science, Kiel University, Kaiserstr. 2, 24143 Kiel, Germany. 2Laboratory of Bio-Inspired and Graphene Nanomechanics, Department of Civil, Environmental and Mechanical Engineering, University of Trento, via Mesiano 77, I-38123 Trento, Italy. 3Functional Morphology and Biomechanics, Zoological Institute, Kiel University, Am Botanischen Garten 1-9, 24098 Kiel, Germany. 4Ket Lab, Edoardo Amaldi Foundation, Italian Space Agency, Via del Politecnico snc, 00133 Rome, Italy. 5School of Engineering and Materials Science, Queen Mary University of London, Mile End Road, London E1 4NS, UK. Correspondence and requests for materials should be addressed to F.S. (email: fas@tf.uni-kiel.de) or to N.M.P. (email: nicola.pugno@unitn.it) or to R.A. (email: ra@tf.uni-kiel.de)
incorporating the unique and exceptional properties of low-dimensional carbon materials like carbon nanotubes (CNTs) into macroscopic functional materials is still very challenging, and this is the reason why their day-to-day application remains limited to the laboratory scale. Nevertheless, CNTs are well known for their high electrical, thermal, optical as well as mechanical properties and thus they are one of the most widely studied materials within the last couple of decades. Different CNT-based assemblies have been reported, including one-dimensional (1D) fibers,2–4 2D films,5–7 buckypapers,8–10 and 3D aerogels.11–15 The latter ones have opened many possibilities for new applications in the field of sensors16,17, catalysis18–20, supercapacitors21,22, as well as free-standing electrodes,23, and recyclable absorbers,18,24,25 mainly due to their extremely large surface to volume ratio, hierarchical porous structural morphology and, most important, the macroscopic dimensions.26

The decisive problem with CNT-based composites with respect to polymer reinforcement is the matrix-filler interaction. Without an effective chemical modification of the CNTs the externally applied stresses to the composite are not directly transferred to the tubes and thus no effective reinforcement takes place. However, the chemical modifications often weaken the structure of the CNTs.9 Hence, a reliable reinforcement can only be achieved with ultra-long unmodified CNTs, which could be done either by welding, knotting, or felting of the individual tubes. The latter can already be realized in the form of 2D buckypapers infiltrated with polymers, leading to an increase in the mechanical properties by a factor of about 3, 9, and 28 with respect to modulus, strength, and toughness, respectively.9 However, buckypaper-reinforced polymers with properties beyond 2D (films/foils/layers) are still missing. A realization of this approach in form of a real 3D composite material is shown here for the first time, to the best of our literature knowledge, leading to unique characteristics in mechanical as well as electrical properties of the stand-alone carbon material and of the resulting composites.

In general, the preparation methods of such 3D CNT networks can be divided into two classes: a dry chemistry (direct growth of CNTs using a chemical vapor deposition process (CVD)) or wet chemistry approach (CNT networks from a CNTs dispersion). The 3D CNT assemblies grown by CVD process show a high mechanical flexibility as well as a high electrical conductivity due to their long individual CNTs, whereas the wet chemistry approaches offer well-controlled reaction conditions, tunable composition, and desired scalability.11,12,25,26 However, both of these processes suffer from certain drawbacks, such as the necessity for a large amount of metal catalyst and the reliability of the reactions involved within the CVD process (e.g., control of the number of stacked, rolled up graphene sheets per CNT).16,27,28 As far as the wet chemistry approaches are concerned, the characteristics of 3D CNT assemblies depend mainly on the quality of the CNT dispersion, leading to many defects and shortening of CNTs resulting from the required ultrasonication steps.11,26,28 There have also been several reports on the fabrication of 3D carbon structures derived from porous templates. These offer the possibility to form open pore structures, with pore sizes up to several microns in diameter. This allows for a tailorable pore-size distribution of macro- or meso-pores, in comparison to the closed pore structures (with pores mostly in the

Fig. 1 Overview of the CNT/T-ZnO composite structure. a Schematic representation of the fabrication process showing the highly porous (93%) ceramic network consisting of pre-sintered tetrapodal shaped ZnO microparticles ($V = 1.7$ cm$^3$) before and after CNT infiltration. By adding CNTs to the network self-entangled CNT networks are formed leading to a high mechanical reinforcement effect, similar to traditional bamboo lashing; b, c SEM images of the ceramic network coated with a homogenous layer of self-entangled carbon nanotubes; d Detail of the CNT network around ZnO tetrapod central joint; e Detail of CNT network around tetrapods junction; f, g High magnification SEM images showing that the CNTs form self-entangled layers on the ceramic template; h, i Self-entangled CNT layer on a broken tetrapod arm, revealing the thickness of the coated CNT layer. (Scale bars: single: 1 $\mu$m, double: 10 $\mu$m)
nanometer range) prepared by most wet-chemistry approaches. For most of the applications, the open pore structures, with pores on the micrometer scale, are highly beneficial, since they allow for a large and especially highly accessible surface area (especially for nanostructured pore surfaces), which is not the case for closed pore structures. However, those template-based methods, which always rely on metal foams (mainly nickel), are based on the direct growth of CNTs by means of CVD and thereby creating not only CNTs but also CNT/graphene composites due to the overlapping growth conditions.

Macroscopically expanded (>cm$^2$ size) and highly porous 3D CNT tube (CNTT) networks are realized by a direct wet chemical infiltration of dispersed CNTs into a porous ceramic network, thereby overcoming most of the drawbacks of other well-known synthesis methods. The infiltrated CNTs form self-entangled networks surrounding the ceramic network in the form of a nanofelted assembly, resulting in a double-hierarchical CNTT architecture. The concept enables the formation of open porous CNTT structures, mechanical reinforced and conductive CNTT/ceramic-, and CNTT/polymer composites. The highly porous (~93%) ceramic becomes significantly reinforced under both tensile (factor of ~40) and compression (factor of ~147) loadings when infiltrated with self-entangled CNTs, being able to support more than 10^5 times their own weight (with length of ~6 mm, porosity >87%). Finite element method (FEM) simulations confirm that in such a hybrid structure, the CNTs are employed in their extraordinary tensile properties, even though the structure is loaded in compression (similar to tensigrency). To the best of our knowledge, such high reinforcement gain has never been shown by any macroscopic 3D CNT composite structure prepared by wet-chemical means. The CNTT assemblies show high conductivity (~130 S m$^{-1}$) at low densities and a higher mechanical stability (~5 times, ultimate compressive strength ~0.25 MPa) in contrast to conventional 3D CNT assemblies due to their self-entangling nature. Additionally, the double-hierarchical structure allows the decrease of the percolation threshold in polymers and enables self-enhancing stretchable conductors. A 3D CNT structure has been realized here for the first time and it exhibits mechanical and electrical properties suitable for a wide range of technologies, including stretchable conductors, gas sensing, cell-scaffold materials, and cathode materials for batteries. In contrast to most other 3D nanocarbon architectures, the structure presented here is an open pore structure with a high porosity and pores in the range of several micrometers, which is beneficial for several applications due to the ease in high surface accessibility.

**Results**

**3D CNTT/ceramic composites.** Fabrication of the 3D composite structures, consisting of CNTs on a ceramic template of a porous interconnected network of ZnO tetrapods (CNTT/t-ZnO), was achieved by a simple dripping method, as illustrated in Fig. 1a. Heated cylindrical pre-sintered highly porous ceramic t-ZnO networks (Supplementary Fig. 1) with a low density of 0.3 g cm$^{-3}$ (porosity >93%) were infiltrated with a commercially available aqueous CNT dispersion using a custom designed computer controlled syringe and dried under ambient conditions (see Supplementary Movie 1). The amount of CNTs was controlled precisely by repeated infiltrations of the template. Representative scanning electron microscopy (SEM) images of the structural morphologies are shown in Fig. 1b–i, revealing the successful coverage of the ceramic 3D network with interwoven layers of self-entangled CNTs.

The detailed SEM study suggests that almost the entire porous network is covered with a homogeneous felted CNT layer (Supplementary Fig. 2) with a thickness ranging from the nano to the submicron scale. The prerequisites for a uniform distribution of CNTs are a highly porous 3D ZnO (as porous as possible, in the present case of ~93% porosity) with a hydrophilic surface as well as the high concentration and dispersion quality of the used CNT ink. It is important to note that these templates have open pores of several µm in diameter. Only thereby is a homogeneous coating possible. A more detailed discussion of the requirements of the template as well as the CNT dispersion etc., can be found in the Supplementary Discussion section. The high porosity of the ceramic leads to large capillary forces upon contact with the CNT ink allowing the liquid to be easily infiltrated and rapidly absorbed. Accordingly, due to the hydrophilic nature of the ceramic network, the aqueous dispersion will maximize its interface area upon CNT infiltration process. Increasing the amount of infiltrated dispersion will increase the wetted interface area and thus the infiltrated volume, up to a point where the entire template is filled with the CNT dispersion (as seen in Supplementary Movie 1). Due to the high porosity of the network no self-filtering effect can be observed, even when the template is already infiltrated with a high CNT load. For the formation of the self-entangled CNT layer, two fundamental mechanisms could be most likely responsible. First, upon infiltration, some CNTs will directly attach to the ZnO surface due to its high polariztion and thus particle-substrate interaction. Surfaces that are already covered with CNTs will barely attach further CNTs due to the stabilizing agents in the CNT dispersion and in the already existing thin water film. Thereby a self-filtering effect is avoided and thus assures a widely homogeneous thin self-entangled CNT film coating (Supplementary Fig. 2) well below 1 µm over several mm penetration into the 3D network (ensuring aspect ratios >10). A more detailed description of the self-entangled layer formation is presented in the Supplementary Discussion together with a 2D model (Supplementary Fig. 3). By repeated infiltration after drying (which reduces the effect of the dispersion agent on the already deposited CNTs), the CNT concentration increases leading to the deposition of thicker CNTTs in the form of felted self-entangled networks (Fig. 1g–i). In the final stage, the drying process tends to transport CNTs in minimal surfaces pronounced at junctions in the ceramic network, which results in the formation of CNT nano-nets spanning between the legs of the tetrapods (Fig. 1e). The thickness of the self-entangled CNT network layers ranges approximately from 50 nm to 1000 nm (Fig. 1h, i), depending on the infiltration time. Samples with different CNT concentrations at places where arms of the tetrapods were broken were investigated (Fig. 1h, g) and the thickness of the CNT layer was measured, which varied only slightly throughout the complete 3D samples. The interwoven CNT networks formed can be compared to the so-called 2D buckypapers, which are sheets made of CNTs (Fig. 1g, i). In general such CNT sheets are formed via the deposition of suspended nanotubes onto a suitable 2D substrate. During drying, the CNTs form highly porous, interwoven networks, consisting of randomly arranged nanotubes, which are held together only by felting and van-der-Waals forces.

In contrast to reported synthesis processes in literature, the present strategy offers a high degree of fabrication diversity and is not limited to the material presented here. In fact, a large number of permutations and combinations (e.g., other 1D and 2D nanomaterials) can be adopted for realizing multifunctional 3D
nanostructures. An example is presented in Supplementary Fig. 4, showing a highly porous 3D polymer structure produced by the same method.

The mechanical and electrical properties of the CNTT/t-ZnO composites are presented in Fig. 2, revealing a surprisingly high compressive strength increase by more than 2 orders of magnitude. Compressive strength has been enhanced by more than a factor of 147, i.e., from 0.017 MPa (equal to a specific strength of ~0.057 MPa cm³ g⁻¹) of the reference ceramic network to almost ~2.5 MPa (equal to ~6.4 MPa cm³ g⁻¹) for the maximum coated network, adding only 25 wt%. The porosity changes from 93 to 87% after infiltration, for the maximum CNT concentration (~0.10 g cm⁻³). However, due to the addition of CNTs, pores in the nanometer range are introduced, next to the large pores (µm-range) of the 3D template. The resulting highly porous CNTT-ceramic 3D composite structure with a height of 6 mm is thus able to carry more than 10⁵ times of its own weight. Some typical stress–strain (compression) behaviors of CNTT/ceramic composites with varying CNT concentration, as well as for that of the pure ceramic (reference) are given in Fig. 2a, b respectively. In Fig. 2c, the maximum compressive strength and the Young’s modulus values are plotted as a function of CNT concentration in the composite for templates having a density of 0.3 g cm⁻³. Additional measurements and discussions regarding the influence of the template density on the mechanical properties of the CNTT/ceramic composites can be found in Supplementary Fig. 5. As depicted, the CNT concentration was varied between 0 and 100 mg cm⁻². Furthermore, before testing all samples were dried overnight to avoid any water contaminations, which could lead to an improvement in the mechanical properties based on capillary forces between the individual particles (CNTs), as well as between the CNTs and the ZnO. Furthermore, we observed, that for templates having a very low density (<0.15 g cm⁻³) repeated infiltration leads to a shrinkage of the template, which might be related to the high capillary forces between the individual CNTs during drying, leading to high tensile forces and thus to the shrinkage of the template (similar to the effect as in the fibers of wet paper)⁴². Moreover, since the aqueous CNT dispersion was stabilized by carboxymethyl cellulose (CMC), measurements of the reference material without CNTs have also been carried out (Fig. 2d). The density of the utilized ceramic was kept constant at 0.3 g cm⁻³ for all the composite specimens, and at least three
samples were measured for each data point shown. From the stress–strain curves it can be clearly seen that both the compressive strength and the Young’s modulus increase with an increasing amount of infiltrated CNTs (Supplementary Table 1). The reason for the drastic increase in compressive strength is mainly attributed to the structured architecture within the composite, converting the compressive stress on the ceramic into tensile strength of the individual CNTs inside the CNTTs. Thus a tensional integrity is formed (tensegrity), which is a structural principle in architecture, based on the use of isolated components in compression inside a net of continuous tension, allowing for a mechanical stable network under compressive stress, by redirecting the force into tension. In such a configuration, the structural collapse is only possible if the cables yield or the rods buckle. The results obtained from FEM simulations closely confirm the enhancement in strength and stiffness with increasing CNT content in the hybrid network, directly related to the amount of infiltration time (Fig. 2c and Supplementary Fig. 6). Infiltration time is related to the thickness of the coating in this model (see Methods for details). Similar to the role of steel rebar in reinforced concrete, the CNT net with their superior mechanical tensile properties can also seen as a reinforcement of the ZnO tetrapods. Moreover, their contribution is maximized, being far from the cross-section centroid. Additionally, the structure of the CNTT/t-ZnO composite can be mimicked and compared to a traditional bamboo lashing, as depicted in Fig. 1a. In general lashing is known as an arrangement of ropes or webbing to combine two or more items into one rigid structure. In case of traditional bamboo lashing, several flexible filaments are wound around the intersecting points of two bamboo sticks, leading to a lightweight framework with a very high structural strength. The same holds true for the here presented CNTT/t-ZnO structure, in which the interconnection points of the individual tetrapodal legs are combined by simple wrapping with webs made of self-entangled CNTs, as shown in Fig. 1d, e. As holds true for traditional lashing techniques, exerting a force onto this branched structure leads to an employment of the ropes/CNTs in tension, even though the specimen is compressed.

**Fig. 3** Overview of the 3D CNTT structures (0.12 g cm$^{-3}$) obtained from CNTT/t-ZnO composites and their electrical and mechanical characteristics. a Schematic representation of the fabrication process, showing the CNTT/t-ZnO structure before and after etching with HCl (1 M in water); b–e SEM images of the resultant 3D CNTT assembly at different magnifications showing a hollow interconnected tubular structure consisting of self-entangled carbon nanotubes (scale bar: 5 µm); f Compressive stress–strain curves for 3D CNTT assemblies showing a high structural strength of up to 0.24 MPa (dots represent experimental measurements, continuous line FEM simulation); g Conductivity (~130 S m$^{-1}$) during compression test; h FEM image showing the tensile behavior of the CNTT arms under a global compressive load, indicating that the CNTs are employed in their tensile properties, even though the structure is compressed.
the SEM investigations of mechanically compressed composites containing higher amounts of CNTs show a different fracture behavior in comparison to the reference networks. Behaving like a clamped cantilever\(^{16}\) and as per our observations, the pure ZnO tetrapods tend to break at the junctions between the central core and the legs, where the maximum stress arises. However, for CNT-coated t-ZnO networks, it could also be observed that individual legs get fractured (Supplementary Fig. 8), which is a clear indication that the entangled CNT networks formed lead to an overall reinforcement of the ceramic micro-architecture, especially at the interconnection points of the tetrapods within the network and thereby redirecting the stress. Furthermore, even if the structure is broken, it does not collapse due to the felted self-entangled CNT network around it (Supplementary Fig. 8). As indicated in Fig. 2a, c the reinforcing effect is rather small for low CNT concentrations. However, the stepwise addition of CNTs increases the self-entanglement and thereby the compressive strength value as well as the Young’s modulus (up to 2.5 MPa normalized by density 6.4 MPa cm\(^3\) g\(^{-1}\)) and 24.5 MPa (normalized by density 62 MPa cm\(^3\) g\(^{-1}\)). From FEM simulations a strength of 16.3 MPa and a tensile modulus of 3.1 GPa was estimated for the formed CNT film. Composite specimens containing only CMC exhibit only a negligible increase in compressive strength.

The self-entangled CNTT structural network not only affects the compressive strength, but also increases the overall tensile response of the ceramic network by nearly two orders of magnitude. In Fig. 2f a direct comparison between a highly infiltrated and a non-coated network under tensile stress is presented. It can be clearly seen that the 3D composite structure exhibits a specific tensile strength of ~0.8 MPa cm\(^3\) g\(^{-1}\) (equal to ~0.3 MPa) whereas the uncoated highly porous ceramic has only a strength of around 0.02 MPa cm\(^3\) g\(^{-1}\) (it should be noted that measuring the tensile properties of such a fragile structures is quite complicated, several samples have been measured showing a tensile strength between 3 × 10\(^{-3}\) and 7 × 10\(^{-3}\) MPa; the highest value is shown here). Furthermore, the specific Young’s modulus increases from ~3 MPa cm\(^3\) g\(^{-1}\) for the reference template to ~112 MPa cm\(^3\) g\(^{-1}\) for the CNTT/t-ZnO composite, which is equal to a factor of ~40 (Supplementary Table 1). It should be also noted, that the strain at which the maximum stress is reached is rather low (~0.7%) when compared to compression (~7%). During tensile testing the self-entangled CNT networks become disentangled. The force that needs to be overcome is mainly attributed to van-der-Waals forces, as in the case of 2D buckypapers\(^9\). However, when those networks are infiltrated with a polymer, even a weak one like Silicone (e.g., PDMS), a 3D composite is formed. Even though no chemical matrix-filler binding exists, the external applied stress will be entirely transferred to the felted structure of the CNTs and thus increasing the mechanical properties at least by the same strength observed for the unfilled CNTTs.

For conductivity measurements 3D CNTT/t-ZnO composite networks with varying CNT concentration (between 0.2 and 10 mg cm\(^{-2}\) in the case of Baytubes DW 55 CM and 0.32–64 mg cm\(^{-3}\) in the case of CarboDis TN) were synthesized and detailed measurements were carried out (Fig. 2e). In both cases, the conductivity \(\sigma\) varies with the CNT concentration \(c\) approximately with a cubic law (\(\sigma \propto c^3\)) and the values ranging from \(1 \times 10^{-6}\) to \(2.6 \times 10^{-2}\) S m\(^{-1}\) at CNT concentrations of \(2 \times 10^{-4}\) and \(1.1 \times 10^{-2}\) g cm\(^{-3}\), respectively. The approximated cubic law is in agreement with theoretical results obtained from statistical percolation theory\(^{47}\). The high conductivities at low CNT concentrations are directly related to the unique structural hierarchy of the network. The template, due to its tetrapod shape, forms already a 3D percolation network. Therefore, only a few CNTs are needed to form a 3D percolation network on the pre-existing network, compared to the case in which the CNTs need to be arranged in the complete volume. Additionally, only a few dead ends (unconnected tetrapodal arms) exist and thus nearly all the surface of the template contributes to the conductivity. This fact changes drastically in the case of other porous structures having many parallel conductive pathways, which do not contribute to the overall conductivity. The pronounced increase in conductivity with increasing CNT concentration is mainly attributed to the increase in the number of interconnection points, leading to the formation of new conductive pathways. At very low CNT concentrations, no ohmic behavior could be observed, indicating that at such concentrations (<2 × 10\(^{-4}\) g cm\(^{-3}\)) no interconnected conductive pathways exist in the complete 3D sample.

### 3D self-entangled CNTT networks

The highly porous 3D CNTT assembly is obtained just by removing the ceramic template of the CNTT/t-ZnO composite using a simple HCl etching process followed by subsequent critical point drying (Fig. 3a). The resultant architecture consists of hollow tube-shaped self-entangled CNT networks (Fig. 3b–e). Thereby, only samples containing at least 0.07 g cm\(^{-3}\) were stable after the drying process, showing a ghost-like 3D assembly of CNTs with very thin tube walls (Supplementary Fig. 9). The treatment of CNTs using HCl is a well-established method for the removal of impurities and causes no damage to the CNTs under mild conditions (1 M HCl was used in this study)\(^{48}\). In Fig. 3f, stress–strain curves for 3D CNTT structures having a CNT concentration of 0.10 g cm\(^{-3}\) and 0.12 g cm\(^{-3}\) are depicted together with results of numerical simulation\(^{49}\). The corresponding conductivity curves for the two samples are presented in Fig. 3g. The conductivity has been nearly constant during uniaxial compression with values ~130 Sm\(^{-1}\). The stress–strain curve shows a linear elastic regime for strains <13%. After that, the ultimate compressive strength is reached with a value of ~0.24 MPa. The highly porous structure (94%) with a length of 6 mm is thus able to bear more than 40,000 times of its own weight. A lower CNT concentration leads to a less stable network (Supplementary Fig. 9), due to less self-entanglement. Compared to the CNTT/t-ZnO composite networks, this value is only one order of magnitude lower, demonstrating that the pure 3D CNTT assembly still exhibits excellent mechanical properties and is able to bear 2.4 kg cm\(^{-2}\), even having a high porosity of ~94%. As mentioned beforehand, the high strength of the network is directly related to the double-hierarchical architecture. FEM simulations shown in Fig. 3h (see also Supplementary Movie 3) reveal that under a global compression scenario the CNTT film shows regions in which tensile forces act on the coating, confirming again that the CNTs are employed in their extraordinary tensile properties. However, after compression the structure is not able to recover its original shape, both due to damage of the CNTT (rearrangements in the CNTs’ network) and to the mutual slip of the tetrapods, strongly increasing the toughness modulus (area under the stress-strain curve). This is also in agreement with the already existing literature reports about other types of 3D CNT assemblies prepared by wet chemical approaches and with aerographite tetrapod networks\(^{11,12}\).

### Stretchable 3D CNTT/polymer composites

Moreover, the availability of such highly porous networks offers the possibility of fabricating new varieties of CNTT based 3D composites. An exemplary case of 3D CNTT/polymer architectures using PDMS is demonstrated here, showing a unique self-enhancing effect in conductivity during cycling based on the double-hierarchical
architecture. The highly conductive and mechanically stable CNTT/t-ZnO composites can be easily infiltrated with appropriate polymers and the ZnO template can be removed if needed, thereby enabling the fabrication of stretchable porous conductors in form of interconnected channels coated with CNTs (Fig. 4a). The channels produced by wet chemical template removal (HCl) are clearly visible, having a layer of felted self-entangled CNTs at their walls (Fig. 4f–g). According to literature no damage to the used elastomer is caused by the etching process. The porosity of the resultant CNTT/polymer composite is in the order of ~7% after etching of the highly porous ceramic template. Due to the low amount of CNTs used for the CNTT/polymer composites, their volume is negligible. In general the electrical conductivity of CNTT/polymer composites depends on several factors, including the type of CNTs (single, double, or multi-walled), as well as on their length, diameter, synthesis method, etc. However, the characteristics of the CNTs used seem to be less important than those of the polymer matrix used and the dispersion methods required to obtain a homogeneous CNT distribution and thereby a low percolation threshold. The larger van-der-Waals interactions between individual CNTs compared to those between polymer-polymer chains often lead to the aggregation and thereby leading to an increase in the percolation threshold.

**Self-enhancing effect in PDMS/CNT composites.** The here shown anisotropic distribution of entangled multi-walled CNTs in the CNTTs can be used to decrease the percolation threshold for all types of castable polymers as was already discussed with respect to the electrical properties of the CNTT/t-ZnO composites, but also another unique mechanism can be observed, such as a self-enhancing effect in conductivity during cyclic stretching. Figure 4c shows the force–strain curve as well as the conductivity until failure of a CNTT/PDMS composite sample. From the graph it can be clearly seen that the conductivity is decreased with increasing elongation of the sample, having an initial conductivity of ~0.52 S m⁻¹. The decrease in conductivity is rather pronounced in the first 3% of elongation, with a conductivity drop of up to ~0.35 S m⁻¹. After that the conductivity decreases more slowly up to the breaking point (at ~60% strain). This behavior can be attributed to the stretching of the felted CNTs. Thereby some interconnection points between the individual CNTs are broken, which leads to an overall decrease in electrical pathways and thus to a decrease in conductivity (Supplementary Fig. 10). This behavior is well known for stretchable conductors. A rather unexpected phenomenon is the increase in conductivity caused by cycling, similar to the work hardening in mechanics. An example is shown in Fig. 4b for a PDMS/CNTT composite having a CNT concentration of 11.3 × 10⁻³ g cm⁻³. It can be directly observed, that the stressed state always shows a lower conductivity compared to the unstressed one, having an initial spread of ~0.15 S m⁻¹. However, when cycling the samples at small elongations (~13%), a self-enhancing effect in conductivity can be observed over time. This effect is higher for the unstressed state, showing an increase in conductivity from ~0.39 S m⁻¹ to ~0.48 S m⁻¹ after 150 cycles, meaning that the conductivity increases by almost 23%. After that, the conductivity stays rather constant. The effect can be also seen in the stressed state, although, it is rather small compared to the unstressed one. The same behavior can be also observed in samples having a lower CNT concentration of 1.8 mg cm⁻³ (Supplementary Fig. 11), showing an initial conductivity of around 0.136 S m⁻¹ which is increased to ~0.15 S m⁻¹ after 150 cycles.

The self-enhancing effect observed is rather unexpected and has not been reported earlier for other stretchable conductors to the best of our literature knowledge. On the contrary, most of the stretchable conductors suffer from a decrease in conductivity after several elongation cycles. For the observed increase in conductivity, we propose the following mechanism as illustrated in Supplementary Fig. 10: in the initial state, there will be only a few conductive pathways through the CNT network. By stretching one of the hollow tubes (with the
CNTs at the walls) in the direction of its length, some of those conductive pathways will be destroyed, leading to a decrease in conductivity during stretching. However, during the stretching, some CNTs will become orientated and aligned along the direction of the applied force. This effect was also observed in other publications. Due to the alignment the interface area between individual CNTs enlarges, leading to higher van-der-Waals forces between the individual CNTs. If the force is released again, the elastomer (PDMS) will retain its original shape, however, due to the higher van-der-Waals forces and alignment between the individual CNTs, some of the CNTs will stay orientated and will not retain their original shape/position. Thereby, new conductive pathways are formed, leading to an increase in the overall conductivity. The more often the sample is stretched, the more CNTs are aligned and the new electric pathways are formed leading to an increase in the overall conductivity. At some point, most of the CNTs are oriented and no further increase in conductivity can be observed upon further cycling. Furthermore, due to the 3D arrangement of pores in the PDMS caused by the tetrapodal template, this effect will only influence some of the CNTs, mainly the ones at the tubes that are oriented in the direction of the applied force. Thus, due to the double-hierarchical structure a unique self-enhancing effect in conductivity can be observed.

Low percolation threshold. In addition, the double-hierarchical structure of the CNTT composite is also a very decisive factor for the observed high conductivities even at low CNT loadings. In Fig. 4d, several literature values for entangled multi-walled CNTs as well as entangled single-walled CNTs in an epoxy matrix are shown (adopted from ref. [7]) and compared to present composites. For the calculations, the density of the multi-walled CNT used was estimated to be $1.4 \, \text{g/cm}^3$. In contrast to all other systems using entangled multi-walled CNTs, the preparation strategy presented here allows for the simple fabrication of highly conductive stretchable conductors, using extremely low CNT concentrations ($1.8 \, \text{mg/cm}^3$). It is very important to mention here, that this remarkably high value of conductivity could be achieved, even using the commercially available CNT dispersion. The high conductivity at such low CNT concentrations can be directly correlated to the structure and the high porosity of the ceramic template. Infiltrating the templates with CNTs results in the formation of conductive pathways only on the surface of the templates. Thus, the volume in which the CNTs need to be distributed to form a percolated network is strongly decreased. This simple strategy enables the formation of conductive pathways even at very low CNT concentrations, reducing the percolation threshold, without the need of complicated mixing and dispersing required by other processes.

Discussion
In summary, a simple strategy for the versatile fabrication of macroscopic highly porous 3D architectures consisting of interconnected tubes made from self-entangled CNTs (CNTT) has been demonstrated. This self-organized process not only allows for the formation of CNTT networks, but also the formation of 3D nano-architechtures from almost any wet chemically dispersed desired nanoscale structure (1D, 2D, etc.). In fact, several different kinds of low-D nanomaterials can be combined in a tube-shaped 3D structure, enabling the fabrication of multifunctional inorganic-carbon-polymer hybrid 3D nano- and micro-architectured materials for advanced applications. Additionally, the ceramic network can be easily removed by simple chemical etching, which offers a lot of nanostructuring opportunities in the direction of new interesting highly porous 3D composites without the need for high temperatures or vacuum equipment. For example: CNTT-ceramic composites, 3D CNTT stand-alone nano-architectures, CNTT-ceramic-polymer, as well as CNTT-polymer composites have been demonstrated. By the formation of self-entangled CNT networks around the highly porous 3D ceramic a nanostructure with mechanical properties based on the principle of tensegrity was introduced. The specific mechanical and electrical properties of the highly ceramic network were enhanced by several orders of magnitude, forming an efficient combination of two material classes. Their complex shaped architecture together with their properties makes them a versatile base and promising candidate for applications in the field of sensors, nano-electronics, and especially metal-free and functional filters.

Moreover, due to its unique double-hierarchical tube-like structure and the high density of CNTs, the stand-alone CNTT structure shows a higher mechanical stability compared to other 3D CNT assemblies reported before that are based on wet chemistry (Supplementary Fig. 12) and can be easily functionalized with other low-D nanomaterials with a lot of potential application, e.g., as an electrode for Li-S batteries or tissue engineering. Furthermore, embedding these 3D buckypaper-like structures into a polymer allows for an improvement in the mechanical properties, even though no chemical matrix-filler binding exists. Finally, the CNTT-polymer composites (e.g., infiltrated with PDMS) can contribute with their remarkable flexibility, stretchability and fatigue resistant properties to the realization of a new generation of electronic devices.

Methods
Fabrication of CNTT/t-ZnO composites, 3D CNTT assemblies, and PDMS/CNTT composites. The t-ZnO ceramic networks used for composite manufacturing were produced by a simple flame transport synthesis. Zinc powder with a grain size of 1–10 mm was mixed with polyvinyl butyral in a mass ratio of 1:2. The mixture was then heated in a muffle furnace with a heating rate of 60 °C min$^{-1}$ up to 900 °C for 30 min. After that a loose powder of typical ZnO tetrapods was obtained, which was pressed into pellets (height $= 4 \, \text{mm}$, diameter $= 6 \, \text{mm}$), having a density of 0.3 g cm$^{-3}$. Reheating the pellets for 5 h at 1150 °C leads to the formation of junctions between the tetrapods. For CNTT/t-ZnO composite preparation, commercial aqueous CNT dispersion (Baytubes DW 55 CM, Bayer MaterialScience) was diluted with water to a CNT concentration of 1% wt. Additional experiments were carried out using other MWNT dispersions, namely CarboByk 9810 (BYK-Chemie) and CarboDis TN (Future Carbon). To disperse the amount of agglomerates, the dispersion was treated with ultrasonication for 20 min before each infiltration step. While being exposed to 40 °C the t-ZnO pellets were infiltrated with the aqueous CNT dispersion using a self-engineered computer-controlled syringe and subsequently dried for at least 1 h. In this case, infiltration means that the templates were completely filled with dispersion, until no more dispersion was taken up by the 3D network. By repeating this process several times the CNT concentration can be adjusted. For the preparation of the 3D CNTT assemblies, the previously prepared CNTT/t-ZnO composites were placed in a 1 M HCl for at least 4 h to remove the template. After that, the samples were washed with deionized water, which was replaced by pure ethanol (5 times washing), which is necessary for the subsequent critical-point-drying process using an EMS 3000.

Preparation of the stretchable porous conductors was carried out by infiltrating CNTT/t-ZnO films ($60 \times 0.05 \, \text{mm}$) with PDMS (Sylgard 184). A pure PDMS blend of 0.5 mm height was added for stability purposes. To get rid of any air inclusions after infiltration, the specimens were degassed in a muffle furnace with a heating rate of 60 °C per h and afterwards cured under ambient conditions at 80 °C in an oven. For the ZnO removal the samples were placed in a 1 M HCl bath for at least 5 days. The etched samples were dried in a vacuum oven for at least 2 days.

Characterization. The morphologies and structure of the different structures were investigated by SEM (Zeiss Supra 55VP). For the measurement of the CNT layer thickness, at least 3 samples were investigated and the layer thickness was measured at the connection of broken tetrapod arms (a result from the SEM preparation). With respect to the electrical measurements, CNTT/t-ZnO composites as well as the pure 3D CNTT assemblies were connected from both sides to copper foil using silver paste to avoid high contact resistance. In analogy to that, films used to make PDMS/CNTT composites were connected with copper foil at both ends prior to PDMS prepolymer infiltration. Electrical properties were measured using as Keithley 2400 in 4-wire sense mode. The mechanical characterization of the CNTT/t-ZnO composites was carried out using a tensile-test machine (Zwick...
6. Xiao, L. et al. Flexible, stretchable, transparent carbon nanotube thin thicknesses were of 0.46, 1.01, and 1.28 the known concentration surface of the ceramic network (and thus the CNTTs) are described as an integrated solid element (spurious modes controlled). The CNT nets covering the 1. Davis, V. A. et al. True solutions of single-walled carbon nanotubes for References

Received: 26 January 2017 Accepted: 11 September 2017
Published online: 31 October 2017

Data availability
The data that support the findings of this study are available from the corresponding authors upon request.

References
1. Davis, V. A. et al. True solutions of single-walled carbon nanotubes for assembly into macroscopic materials. Nat. Nanotechnol. 4, 830–834 (2009).
2. Ericson, L. M. et al. Macroscopic, neat, single-walled carbon nanotube fibers. Science 305, 1447–1450 (2004).
3. Li, Y.-L., Kinloch, I. A. & Winstead, A. H. Direct spinning of carbon nanotube fibers from chemical vapor deposition synthesis. Science 304, 276–278 (2004).
4. Wang, X. et al. High-ampacity power cables of tightly-packed and aligned carbon nanotubes. Adv. Funct. Mater. 24, 3241–3249 (2014).
5. Shi, Z. et al. Ultrastiff separation of emulsified oil/water mixtures by ultrathin free-standing single-walled carbon nanotube network films. Adv. Mater. 25, 2422–2427 (2013).
6. Xiao, L. et al. Flexible, stretchable, transparent carbon nanotube thin film loudspeakers. Nano Lett. 8, 4539–4545 (2008).
7. Zhang, M. et al. Strong, transparent, multifunctional, carbon nanotube sheets. Science 309, 1215–1219 (2005).
8. Che, J., Chen, P. & Chan-Park, M. B. High-strength carbon nanotube buckypaper composites as applied to free-standing electrodes for supercapacitors. J. Mater. Chem. A 1, 4057 (2013).
9. Coleman, J. N., Khan, U. & Gun'ko, Y. K. Mechanical reinforcement of polymers using carbon nanotubes. Adv. Mater. 18, 689–706 (2006).
10. Roy, S. et al. Formation of carbon nanotube bucky paper and feasibility study for filtration at the nano and molecular scale. J. Phys. Chem. C 116, 19025–19031 (2012).
11. Bryning, M. B. et al. Carbon nanotube aerogels. Adv. Mater. 19, 661–664 (2007).
12. Kim, K. H., Oh, Y. & Islam, M. F. Graphene coating makes carbon nanotube aerogels superelastic and resistant to fatigue. Nat. Nanotechnol. 7, 562–566 (2012).
13. Guo X. et al. Carbon nanotube sponges. Adv. Mater. 22, 617–621 (2010).
14. Shan, C. et al. Three-dimensional nitrogen-doped multilayer carbon nanotube sponges with tunable properties. Nano Lett. 13, 5514–5520 (2013).
15. Ozden, S. et al. Density variant carbon nanotube interconnected solids. Adv. Mater. 27, 1842–1850 (2015).
16. Dong, X. et al. Synthesis of graphene–carbon nanotube hybrid foam and its use as a novel three-dimensional electrode for electrochemical sensing. J. Mater. Chem. 22, 17044 (2012).
17. Wang, M. et al. Modifying native nanocellulose aerogels with carbon nanotubes for mechanoresponsive conductivity and pressure sensing. Adv. Mater. 25, 2428–2432 (2013).
18. Zhang, Z. et al. Bifunctional nanocatalyst based on three-dimensional carbon nanotube–graphene hydrogel supported Pd nanoparticles. one-pot synthesis and its catalytic properties. ACS Appl. Mater. Interfaces 6, 21035–21040 (2014).
19. Li, H. et al. Photocatalytic, recyclable CdS nanoparticle-carbon nanotube hybrid sponges. Nano Res. 5, 265–271 (2012).
20. Skalsitas, T., Avgourgopulos, G. & Tasis, D. Impact of the fabrication method on the physicochemical properties of carbon nanotube-based aerogels. Microporous Mesoporous Mater. 143, 451–457 (2011).
21. Zhang, L. L. & Zhao, X. S. Carbon-based materials as supercapacitor electrodes. Chem. Soc. Rev. 38, 2520–2531 (2009).
22. Wang, W. et al. Three dimensional few layer graphene and carbon nanotube foam architectures for high fidelity supercapacitors. Nano Energy 2, 294–303 (2013).
23. Arici, A. S., Bruce, P., Scrosati, B., Tarascon, J.-M. & van Schalkwijk, W. Nanostructured materials for advanced energy conversion and storage devices. Nat. Mater. 4, 366–377 (2005).
24. Gui, X. et al. Recyclable carbon nanotube sponges for oil absorption. Acta Mater. 59, 4798–4804 (2011).
25. Sun, H., Xu, Z. & Gao, C. Multifunctional, ultra-flyweight, synergistically assembled carbon aerogels. Adv. Mater. 25, 2534–2560 (2013).
26. Du, R., Zhao, Q., Zhang, N. & Zhang, J. Macroscopic carbon nanotube-based 3D monoliths. Small 11, 3263–3289 (2015).
27. Tessonnier, J.-P. & Su, D. S. Recent progress on the growth mechanism of carbon nanotubes: a review. ChemSusChem 4, 824–847 (2011).
28. Zou, J. et al. Ultralight multilayer carbon nanotube aerogel. ACS Nano 4, 7393–7398 (2010).
29. Chen, Z. et al. Three-dimensional flexible and conductive interconnected graphene networks grown by chemical vapour deposition. Nat. Mater. 10, 424–428 (2011).
30. Dong, X. et al. Superhydrophobic and superoleophilic hybrid foam of graphene and carbon nanotube for selective removal of oils or organic solvents from the surface of water. Chem. Commun. (Camb.) 48, 10660–10662 (2012).
31. Li, Y. et al. Highly comformable macroporous graphene monoliths via an improved hydrothermal process. Adv. Mater. 26, 4789–4793 (2014).
32. Mecklenburg, M. et al. Aerographite: ultra lightweight, flexible nanowall, carbon microtube material with outstanding mechanical performance. Adv. Mater. 24, 3486–3490 (2012).
33. Mishra, Y. K. et al. Fabrication of macroscopically flexible and highly porous 3D semiconductor networks from interpenetrating nanostructures by a simple flame transport approach. Particle Particle Syst. Charact. 30, 775–783 (2013).
34. Liu, L., Ma, W. & Zhang, Z. Macroscopic carbon nanotube assemblies. Preparation, properties, and potential applications. Small 7, 1504–1520 (2011).
35. Dong, X. et al. Synthesis of graphene–carbon nanotube hybrid foam and its use as a novel three-dimensional electrode for electrochemical sensing. J. Mater. Chem. 22, 17044 (2012).
36. Mishra, Y. K. et al. Versatile fabrication of complex shaped metal oxide nanostructures and their interconnected networks for multifunctional applications. KONA Powder and Part. J. 31, 92–110 (2014).
37. Jin, X. et al. Study of tetrapodal ZnO-PDMS composites: a comparison of fillers shape in stiffness and hydrophobicity improvements. PLoS ONE 9, e106991 (2014).
38. Tian, D., Zhang, X., Zhai, J. & Jiang, L. Photocontrollable water permeation on the micro/nanoscale hierarchical structured ZnO mesh films. Langmuir 27, 4265–4270 (2011).
39. Choi, D. Y. et al. Highly conductive, bendable, embedded ag nanoparticle wire arrays via convective self-assembly, hybridization into ag nanowire transparent conductors. Adv. Funct. Mater. 25, 3888–3898 (2015).
ARTICLE

40. Jenkins, J., Flickinger, M. & Velev, O. Continuous convective-sedimentation assembly of colloidal microsphere coatings for biotechnology applications. Coatings 3, 26–48 (2013).

41. Wei, Z. & Zhao, Y.-P. Growth of liquid bridge in AFM. J. Phys. D Appl. Phys. 40, 4368–4375 (2007).

42. van de Ven, T. G. M. Capillary forces in wet paper. Ind. Eng. Chem. Res. 47, 7250–7256 (2008).

43. Skelton, R. E., Adhikari, R., Pinaud, J.-P., Chan, W. & Helton, J. W. in Proceedings of the 40th IEEE Conference on Decision and Control, 5, 4254–4259 (IEEE, 2001).

44. Díezán, K. & Clouton, P. L. Building with bamboo. A review of culm connection technology. J. Green Build. 8, 83–93 (2013).

45. Widyowijatnoko, A.

46. Hoffmann, S. et al. Measurement of the bending strength of vapor-liquid-solid grown silicon nanowires. Nano Lett. 6, 622–625 (2006).

47. Bauhofer, W. & Kovacs, J. Z. A review and analysis of electrical percolation in carbon nanotube polymer composites. Compos. Sci. Technol. 69, 1486–1498 (2009).

48. Datyuk, V. et al. Chemical oxidation of multiwalled carbon nanotubes. Carbon 46, 833–840 (2008).

49. Meija, R. et al. Nanomechanics of individual aerographte tetrapods. Nat. Commun. 8, 14982 (2017).

50. Jiao, K., Graham, C. L., Wolff, J., Iyer, R. G. & Kohli, P. Modulating molecular and nanoparticle transport in flexible polydimethylsiloxane membranes. J. Membr. Sci. 401–402, 25–32 (2012).

51. Mata, A., Fleischman, A. J. & Roy, S. Characterization of polydimethylsiloxane (PDMS) properties for biomedical micro/nanosystems. Biomed. Microdevices 7, 281–293 (2005).

52. Spitalsky, Z., Tasis, D., Papagelis, K. & Galiotis, C. Carbon nanotube–polymer composites. Chemistry, processing, mechanical and electrical properties. Prog. Polym. Sci. 35, 357–401 (2010).

53. Gojny, F., Wichmann, M., Friedler, B. & Schulte, K. Influence of different carbon nanotubes on the mechanical properties of epoxy matrix composites–A comparative study. Compos. Sci. Technol. 65, 2300–2313 (2005).

54. Chen, Z. et al. Three-dimensional flexible and conductive interconnected graphene networks grown by chemical vapour deposition. Nat. Mater. 10, 424–428 (2011).

55. Kim, K. H., Vural, M. & Islam, M. F. Single-walled carbon nanotube aerogel-based elastic conductors. Adv. Mater. 23, 2865–2869 (2011).

56. Le Cai et al. Highly transparent and conductive stretchable conductors based on hierarchical reticulate single-walled carbon nanotube architecture. Adv. Funct. Mater. 22, 5238–5244 (2012).

57. Park, J. et al. Three-dimensional nanonetworks for giant stretchability in dielectrics and conductors. Nat. Commun. 3, 916 (2012).

58. Yu, Y. et al. Ultra-stretchable conductors based on buckled super-aligned carbon nanotube films. Nanoscale 7, 10178–10185 (2015).

59. Zhang, X., Yu, X., Zhao, J. & Li, Q. in Carbon Nanotubes—Current Progress of their Polymer Composites (eds Berber M. R. & Hafez I. H.) (InTech, 2016).

60. Yu, Y. et al. Flexible and transparent strain sensors based on super-aligned carbon nanotube films. Nanoscale 9, 6716–6723 (2017).

61. Belytschko, T., Liu, W. K., Moran, B. & Elkhodary, K. I. Nonlinear finite elements for continua and structures (Wiley, 2014).

Acknowledgements

R.A. gratefully acknowledges partial project funding by the Deutsche Forschungsgemeinschaft (DFG) contract AD183-17-1 as well as in the framework of the GRK 2154 and FOR 1616, and support from the European Comission in the framework of the Graphene FET Flagship. N.M.P. is supported by the European Research Council ERC PoC 2015 SILKENE No. 693670 and by the European Comission H2020 under the Graphene FET Flagship (WI4 “Polymer Composites” No. 696656) and under the FET proactive (“Neurofibres” No. 732344). S.S. acknowledges financial support from SILKENE. This work was partly supported by the Leverhulme Trust project CARBTRIB to S.N.G. We acknowledge financial support by Land Schleswig Holstein within the funding program “Open Access Publikationsfonds”. Furthermore, we thank Heather Cavers for proofreading and correcting the manuscript.

Author contributions

F.S., Y.K.M., R.A. and N.M.P. designed the study. F.S., H.K., S.R. and D.S. fabricated the different CNTT samples. S.N.G. provided the critical-point-dryer. F.S., R.A., S.K., S.S. and N.M.P. analyzed the mechanical data. S.S. developed the computational models. F.S., S.S., Y.K.M., S.N.G., N.M.P. and R.A. finalized the study and wrote the paper. All authors have reviewed the manuscript.

Additional information

Supplementary Information accompanies this paper at https://doi.org/10.1038/s41467-017-01324-7.

Competing interests: The authors declare no competing financial interests.

Reprints and permission information is available online at http://npg.nature.com/reprintsandpermissions/

Change history: A correction to this article has been published and is linked from the HTML version of this paper.

Publisher’s note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2017
Supplementary Figure 1. Overview of the t-ZnO template. a,b,c,d) SEM images of the highly porous 3D template consisting of interconnected tetrapodal shaped ZnO particles, fabricated by a simple flame-transport synthesis with a mean diameter of around 25 µm and arm thicknesses of only a few micrometers; e) Junctions between the particles formed during sintering; f) High magnification SEM of a single tetrapod arm
Supplementary Figure 2. Crossectional SEM investigation over a complete CNTT/t-ZnO 3D structure at different magnifications: The sample (height: 6mm, radius: 6mm) was infiltrated 12 times using a 0.5 wt% CNT dispersion (CarboDis TN). For the investigation, the sample was cut in the middle using a razor blade. The different areas indicate, that the coating of the template using the infiltration process is homogenous, even in the middle of the template (no self-filtering effect). Please note, that by cutting the sample, parts of the network get broken (e.g. detached CNT layers, broken tetrapod arms)
Supplementary Figure 3. Schematic illustration of the CNTT coating process. After infiltration with the CNT dispersion, the network is in the filled state (all pores are filled with CNT dispersion). As a result of the high porosity and the large pore sizes of the template the CNT concentration is the same all over the 3D structure. Due to the polarized surface of the ZnO some CNTs get directly attached (particle-substrate force) to it. Upon water evaporation, several menisci are formed between the interconnection points of the template. Due to evaporation losses, an outward fluid flow carries the dispersed particles to the pinned contact line of the meniscus. In this region, the particles start to form a homogenous layer due to immersion capillary forces and particle-substrate force (similar to convective self-assembly). This ensures a widely homogenous coating all over the 3D template structure. On top of that, spanning CNT nets between the interconnection points can be formed because of an increase in CNT concentration in the remaining water during drying.
Supplementary Figure 4. Porous 3D interconnected polymer (PVDF) network after template removal.
Supplementary Figure 5. Compressive Stress (normalized by density) vs. CNT concentration for different densities of the ZnO template for different MWCNT dispersions: a) Comparative plot between different MWCNT dispersions (CarboByk 9810 CarboDis TN, Baytubes DW 55 CM). The graph shown for the Baytubes is the same as shown in Figure 2c of the manuscript; b) CNTT reinforcement effect vs. CNT concentration with respect to the density of the template when a 1wt% CarboDis TN dispersion was used for the infiltration; c) CNTT reinforcement effect vs. CNT concentration with respect to the density of the template when a 0.5wt% CarboDis TN dispersion was used for the infiltration; d) CNTT reinforcement effect vs. CNT concentration with respect to the density of the template when a 0.5wt% CarboByk 9810 dispersion was used for the infiltration; e) CNTT reinforcement effect vs. CNT concentration for different CarboDis TN concentrations in the dispersion used for the infiltration (template density 0.3 g cm$^{-3}$); f) CNTT reinforcement effect vs. CNT concentration for different CarboByk 9810 concentrations in the dispersion used for the infiltration (template density 0.3 g cm$^{-3}$).
Supplementary Figure 6. Detail of compression experiments on t-ZnO network (see Figure 2). Blue dots represents experimental data while the black line is the result from FEM simulations. Snapshot of simulation at 4 different deformation levels are shown.
Supplementary Figure 7. Comparison between the pure template and a template containing 0.1 g cm$^{-3}$ carbon nanotubes after compression showing that the carbon nanotube coating leads to a higher restoring force (scale bar: 3 mm). The whole compression experiment is shown in Video S2.
Supplementary Figure 8. Fractures sites of a t-ZnO/CNTT composite after compression: a-b) Fractures between the core and a leg of a tetrapod, which are still hold together by the carbon nanotubes; c) enlarged fracture site from b; d-e) Fractures inside the leg of a tetrapod; f) Fracture at the core of a tetrapod. g-h) Detail of FEM simulation showing the stress distribution at the t-ZnO/CNTT tetrapod joint which causes CNNT film failure. Elements of the film (in yellow) are eroded due to reach of the failure limit letting the t-ZnO below (in red) to be visible.
Supplementary Figure 9. 3D CNTT assembly at different magnifications: a-b) CNTT network (100 mg cm\(^3\)) at low magnifications, showing the interconnected tubes; c-d) CNTT assembly having a density of 70 mg cm\(^3\).
Supplementary Figure 10. Schematic illustration of the self-enhancing effect during cyclic stretching of the CNTT/PDMS composite structures. In the initial state, only a few conductive pathways exist throughout the 3D composite. Upon stretching, the CNTs get unidirectional oriented and aligned in the direction of the applied force. On top of that, some pathways will be broken, leading to a lower conductivity in the stretched state. Thereby the interface area between individual CNTs becomes higher, resulting in large van-der Waals forces (as indicated by the red markers). Upon retraction, some of the CNTs will not recover their original shape, especially at the new formed interconnection points, leading to an increase in conductive pathways.
Supplementary Figure 11. Mechanical and electrical properties of a porous stretchable conductor having a carbon nanotube concentration of $1.8 \times 10^{-3}$ g cm$^{-3}$.
Supplementary Figure 12. Comparison of 3D carbon nanotube and graphene assemblies prepared by wet chemistry\textsuperscript{1–10}. The CNTT architecture has a higher mechanical strength under compression.
## Supplementary Table

### Supplementary Table 1. Mechanical Properties of different CNTT structures

| Sample          | Density (ZnO) g/cm³ | Density (CNT) g/cm³ | Compressive Strength MPa | Specific Compressive Strength MPa*cm³/g | Young's Modulus (Comp.) MPa | Specific Young's Modulus (Comp.) MPa*cm³/g | Tensile Strength MPa | Specific Tensile Strength MPa*cm³/g | Young's Modulus (Tensile) MPa | Specific Young's Modulus (Tensile) MPa*cm³/g |
|-----------------|---------------------|---------------------|--------------------------|----------------------------------------|----------------------------|---------------------------------------------|---------------------|--------------------------------------|-------------------------------------|-------------------------------------------|
| t-ZnO           | 0.300               | 0.000               | 0.017                    | 0.057                                  | 0.574                      | 1.916                                       | 0.007               | 0.02                                 | 0.887                               | 2.957                                     |
| t-ZnO/CNTT      | 0.300               | 0.020               | 0.060                    | 0.186                                  | 1.126                      | 3.519                                       | -                   | -                                    | -                                   | -                                         |
| t-ZnO/CNTT      | 0.300               | 0.034               | 0.203                    | 0.609                                  | 4.286                      | 12.832                                      | -                   | -                                    | -                                   | -                                         |
| t-ZnO/CNTT      | 0.300               | 0.047               | 0.402                    | 1.159                                  | 6.678                      | 19.246                                      | -                   | -                                    | -                                   | -                                         |
| t-ZnO/CNTT      | 0.300               | 0.074               | 1.271                    | 3.397                                  | 17.45                      | 46.673                                      | -                   | -                                    | -                                   | -                                         |
| CNTT            | 0.000               | 0.100               | 0.194                    | 1.940                                  | 2.152                      | 21.520                                      | -                   | -                                    | -                                   | -                                         |
| CNTT            | 0.000               | 0.120               | 0.233                    | 1.942                                  | 2.166                      | 18.050                                      | -                   | -                                    | -                                   | -                                         |
Supplementary Discussion

Main factors that govern the formation of the CNT self-entangled structure

1. Template

First of all the template needs to be highly porous, having an open pore structure, with a pore size diameter that is larger compared to the largest dimension of the particle by at least one order of magnitude to allow for the infiltration of particles, thus nano to sub-micro. This is only the case in open pore structures, as the one used in this study. On top of that, this is especially true for nanotubes, due to their large size in one dimension. With increasing template density, the porosity decreases drastically, resulting in smaller pore diameters. In return, this will hinder the formation of a homogeneous coating and thus reinforcement effect, due to the fact, that the CNTs in their dispersed form will not effectively enter into the entire template because of the reduced pore size. Depending on the length of the CNTs a filtering effect will occur, which increases with increasing number of infiltrations. Therefore, higher densities of the template were not considered and 0.3 g cm\(^{-3}\) was chosen as the optimum density with a better compromise in terms of its mechanical strength (the pure template is rather soft and thus hard to handle) and porosity (~94%). Thus, a certain pore size (in the \(\mu\text{m}\) range) is definitely required to enable a homogenous CNT. However, templates having a density of less than 0.15 g cm\(^{-3}\) i.e., with high porosity (>95%), are compressed by the capillary action during CNT infiltration, resulting in a too low mechanical stability of the pure template. They are so fragile that during infiltration, cracks are introduced which lead to a complete collapse of the template’s network architecture after several infiltrations.

Another requirement for a homogenous coating (in the case of aqueous dispersions) is the hydrophilicity of the template. Only templates with super-hydrophilic properties will allow for a homogenous coating, since in this case the water spreads over the whole surface due to surface energy minimization. In our case, all these requirements are fulfilled for templates having densities in the range of 0.15 g cm\(^{-3}\) to 0.3 g cm\(^{-3}\). Templates having a density lower than 0.15 g cm\(^{-3}\) do suffer shrinkage due to their low stability. The influence of the template density on the mechanical properties of the resulting composite materials is shown in Supplementary Figure 5 and discussed in more detail in the following paragraph.

2. Concentration of the used dispersion and kind of nanomaterial

The concentration plays a crucial role when trying to infiltrate the highly porous networks. In most cases, the concentration of the dispersion is limited by the material itself and not by the infiltration process, e.g. how much of the solid can be dispersed
without destabilization. In the case of CNTs, the concentration needs to be adjusted carefully. We have found, that a concentration of around 1 wt% is a good choice for most dispersions. However, this value depends mainly on the dispersion quality and the used CNTs (length, diameter etc.). In general, to high concentrations will increase the formation of agglomerates and nets between the junctions of the template, thereby causing an inhomogeneous coating. To avoid agglomerates, the dispersion should be ultrasonificated before each infiltration step. A lower CNT concentration will form more homogenous layers, however, the infiltration steps will increase to achieve a sufficient coating thickness in terms of mechanical stability, which is unwanted in most cases. On top of that, we observed, that by using CNT dispersions which are low concentrated the entanglement between the individual CNTs will be lower, resulting in a lower reinforcement effect. Every infiltration step will produce a new CNT layer, which is not entangled with the one beneath. Thus, we decided to decrease the concentration to such a level, that we still have a very homogenous coating but the highest degree of entanglement possible with only small deviations in the layer thickness. When using other CNT dispersions, the concentration needs to be adjusted accordingly. Furthermore, the length of the individual CNTs needs to be considered, as mentioned in the description of the template properties.

On top of that, we observed, that the process is self-regulated. After the template is infiltrated several times with CNT dispersion (thus containing a certain amount of CNTs), all the surface is coated at one point. At this point, the structure is not able to take up anymore dispersion and, what is most important: it does not take up any water at all. Therefore, this effect is not related to a self-filtering effect, but can be directly attributed to the shielding of the polarity of the ZnO by the CNT coating, which reduces the hydrophilicity and thus makes it impossible for the template to take up more water. Thereby, the layer thickness can only be enlarged up to a certain point and no complete filling of the template pores is possible. This effect also ensures a widely homogenous coating throughout the 3D structure. Additionally, we observed, that when templates with different densities were infiltrated with the same CNT dispersion, that at lower template densities, this effect started earlier, compared to higher density templates, which can be attributed to the lower surface area that needs to be coated for smaller densities.

For the here presented process we investigated three different commercially available MWCNT dispersions, namely CarboByk 9810 (BYK-Chemie), CarboDis TN (Future Carbon), and Baytubes DW 55 CM (Bayer MaterialScience). All the experiments and results shown in the main manuscript (and if not state elsewise) were done by using Baytubes DW 55 CM. This dispersion was found to give the best results in terms of mechanical reinforcement und structural homogeneity (Supplementary Figure 5). As illustrated in Supplementary Figure 5a, the reinforcement effect is different for the
different CNT dispersions. In the case of CarboDis TN, the effect was even higher compared to the measurements shown in the main manuscript (Baytubes). However, the samples were already saturated at smaller CNT concentrations, resulting in an overall smaller reinforcement effect. On the other hand, using CarboByk, a high amount of CNTs could be infiltrated into the ceramic networks; however, the reinforcement effect was rather low compared to CarboDis TN and Baytubes. We observed, that CarboByk 9810 (diluted to 1 wt%) tends to form a lot of agglomerates next to the coating around the template, resulting in a non uniformity of the films. In the case of CarboDis TN, the CNT coating was very homogenous, similar to the one formed when using Baytubes DW 55 CM. A SEM investigation of the homogeneity is shown in Supplementary Figure 2. Therefore, the used CNT dispersion plays a critical role in the reinforcement effect (stabilizing agent, CNT length, CNT diameter etc.). In Supplementary Figure 5b,c,d the effect of the template density is illustrated for different CNT dispersions and concentrations. Form Supplementary Figure 5b it can be observed, that the normalized compressive stress for low CNT concentrations is higher with higher template density. With increasing CNT concentration in the ceramic networks, this trend changes and at high CNT concentrations (0.05 g cm\(^{-3}\)) the normalized compressive stress is highest for the lowest template density. This might be directly related to the fact, that in the case of the lower template density, less ZnO surface is available and thus at the same CNT loading, the thickness of the formed self-entangled CNT layer is higher. A similar trend is shown in Supplementary Figure 5c. In contrast to those measurements, when using CarboByk 9810 as the infiltration dispersion, such an effect is not observed. The highest template density has always the highest normalized compressive stress. Again, this is related to the high amount of agglomerates formed when using this dispersion. Furthermore in Supplementary Figure 5e,f the effect of CNT concentration in the dispersion is illustrated. There is no change in the case of CarboByk (Supplementary Figure 5f), which is again a result of the inhomogeneous coating process and high amount of agglomerates. In the case of CarboDis TN there is a big difference between templates coated with a 0.5 wt% or 1 wt% dispersion. At first glance, this effect is unexpected: By infiltrating the ceramic template with a low wt% CNT dispersion one might expect to form a more homogenous coating compared to a higher concentrated one. Even though this might be the case, the self-entanglement is much higher in the case of a higher CNT concentration in the dispersion. In other words, when we have one self-entangled CNT layer on a substrate (dried state) and we apply another CNT coating. There is no entanglement between those two layers. However, if we directly use a higher concentrated CNT dispersion to form a film of same thickness, the self-entanglement will be the same throughout the whole film, thus leading to higher mechanical properties.

(Please note: a special designed CNT dispersion might lead to a much higher effect.)
3. Infiltration methods

As by our observations, the infiltration method itself has no influence on the formed structure. As shown in our supporting video S1, the sample is infiltrated from the top (as it was the case for all samples for this manuscript). However, this was simply done for simplicity of the process. Due to the large capillary forces and the hydrophilicity of the template, it is also possible to infiltrate the template from every side or just by placing it on a drop of dispersion. However, this has no effect on the formed CNTT assembly. Furthermore, the temperature at which the samples are dried has an influence. Higher temperatures lead to faster water evaporation and thus to a more inhomogeneous self-assembly of the CNTs. However, at low temperatures, the water will only slowly evaporate and even some residues might stay in the network, which might hinder the complete filling in the next infiltration step. We found, that temperatures of around 50 °C lead to better results in terms of CNT self-assembly.
Supplementary References

1. Dong, L. et al. Facile preparation of carbon nanotube aerogels with controlled hierarchical microstructures and versatile performance. Carbon 90, 164–171 (2015).

2. Hu, H., Zhao, Z., Wan, W., Gogotsi, Y. & Qiu, J. Ultralight and highly compressible graphene aerogels. Advanced Materials 25, 2219–2223 (2013).

3. Kohlmeyer, R. R., Lor, M., Deng, J., Liu, H. & Chen, J. Preparation of stable carbon nanotube aerogels with high electrical conductivity and porosity. Carbon 49, 2352–2361 (2011).

4. Xu, Y., Sheng, K., Li, C. & Shi, G. Self-assembled graphene hydrogel via a one-step hydrothermal process. ACS Nano 4, 4324–4330 (2010).

5. Kim, K. H., Oh, Y. & Islam, M. F. Graphene coating makes carbon nanotube aerogels superelastic and resistant to fatigue. Nat. Nanotechnol. 7, 562–566 (2012).

6. Kim, K. H., Oh, Y. & Islam, M. F. Mechanical and Thermal Management Characteristics of Ultrahigh Surface Area Single-Walled Carbon Nanotube Aerogels. Advanced Functional Materials 23, 377–383 (2013).

7. Sun, H., Xu, Z. & Gao, C. Multifunctional, ultra-flyweight, synergistically assembled carbon aerogels. Advanced Materials 25, 2554–2560 (2013).

8. Zou, J. et al. Ultralight multiwalled carbon nanotube aerogel. ACS Nano 4, 7293–7302 (2010).

9. Bryning, M. B. et al. Carbon Nanotube Aerogels. Advanced Materials 19, 661–664 (2007).

10. Peng, Q. et al. Graphene nanoribbon aerogels unzipped from carbon nanotube sponges. Adv. Mater. 26, 3241–3247 (2014).
Description of Additional Supplementary Files

**File name:** Supplementary Movie 1

**Description:** 3D ceramic templates are infiltrated with an aqueous carbon nanotube dispersion using a custom designed computer controlled syringe setup and dried under ambient conditions on a hot plate (40 °C). During infiltration, the aqueous carbon nanotube dispersion is maximizing its interface area because of the hydrophilic surface of the template. When the first drop of CNT dispersion gets in contact with the ceramic template, it will penetrate a certain volume of the template, namely the volume that is needed to maximize its surface area, because of the hydrophilic properties of the template. Following droplets will increase this volume (more surface area is needed). Thus, at some point the template is completely filled with dispersion and increasing the amount will lead to the formation of a drop forming on top of the template surface. Using a template with a density of 0.3 g cm\(^{-3}\) (94% porosity) and a volume of 0.17 cm\(^{3}\) the free volume is equal to around 0.16 cm\(^{3}\). Thus, the template should be able to take up 160 µl of water before a droplet forms on the top surface, which indeed is the case. Therefore, after infiltration, the whole network is flooded and due to the high porosity of the network, the CNT concentration can be assumed to be constant all over the sample. Furthermore, it has to be pointed out, that the flow rate of the CNT dispersion through the template seems to be non-homogenous. Indeed, it is very homogenous but appears to be different due to very tiny variations in the pore sizes of the ceramic template. Pores, which are a little closer provide higher capillary forces and are thus chosen to be wetted first by the CNT dispersion. Subsequent liquid droplets wet homogenous the non-wetted areas. This is also shown by the fact, that there is no filtering effect visible. After complete infiltration, the sample has a homogenous color (there is no black area on top, which gets greyer when moving down).

(Note: The Video shows only the first infiltration in real time).

**File name:** Supplementary Movie 2

**Description:** As was shown in Video S1, the ZnO template is infiltrated with a 0.5 wt% CNT dispersion for one time (complete infiltration). Afterwards, the infiltrated sample is moved directly (no drying time) into a beaker filled with distilled water. Upon water contact, the CNT dispersion in the template is not mixing with the surrounding water. Only a small amount of CNTs are removed from the template, even when the mixture is stirred. As a comparison, if the same amount of CNT dispersion (as was added to the pure template) is mixed with the water, the color change is very strong. This proves the fact, that there is some certain interaction between the CNTs and the ZnO template, though which the CNTs get distributed homogenously on the ZnO surfaces.

**File name:** Supplementary Movie 3

**Description:** Compression tests on a reference 3D ceramic template (right) and a template containing 0.1 g/cm\(^{3}\) carbon nanotubes (left). After the force is removed, the carbon nanotube containing structure shows a higher restoring force compared to the pure template, thereby indicating
that individual carbon nanotubes in the CNTT structure get employed in their tensile properties, even though the sample is compressed.

File name: Supplementary Movie 4
Description: Compression tests on a reference 3D CNTT network of 0.10 g cm⁻³ carbon nanotubes. The load is applied along the vertical directions in the video. Contour plot of the elastic strain is shown. It clearly appears how the tubes are employed in bending and in tension under a compressive load on the specimen. Analogously to aerographite tetrapodal networks previously studied by the authors, the deformation behavior of the entangled CNTT network is governed by the formation of buckling hinges at tetrapod joints or within the arms. The latter are prone to appear in the proximity in the entangling joints between different tetrapods.
Publisher Correction: Hierarchical self-entangled carbon nanotube tube networks

Fabian Schütt1, Stefano Signetti2, Helge Krüger1, Sarah Röder1, Daria Smazna1, Sören Kaps1, Stanislav N. Gorb3, Yogendra Kumar Mishra1, Nicola M. Pugno2,4,5 & Rainer Adelung1

Correction to: Nature Communications https://doi.org/10.1038/s41467-017-01324-7, Article published online 31 October 2017

The original version of this Article was missing the ORCID ID of Professor Nicola Pugno.

Also in the original version of this Article, the third to last sentence of the fourth paragraph of the Results incorrectly read "However, the stepwise addition of CNTs increases the self-entanglement and thereby the compressive strength value as well as the Young’s modulus (up to 2.5 MPa (normalized by density 6.4)) and 24.5 MPa (normalized by density 62 MPa cm3 g-1))." The correct version adds the units "MPa cm3 g-1" to "6.4".

Finally, in the original version of this Article, the y-axis label of Fig. 3f incorrectly read "Comp. strengthy". The new version corrects that to "Comp. Strength".

These errors have now been corrected in both the PDF and the HTML versions of the Article.

Published online: 09 January 2018

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2018

1 Functional Nanomaterials, Institute for Materials Science, Kiel University, Kaiserstr. 2, 24143 Kiel, Germany. 2 Laboratory of Bio-Inspired and Graphene Nanomechanics, Department of Civil, Environmental and Mechanical Engineering, University of Trento, via Mesiano 77, I-38123 Trento, Italy. 3 Functional Morphology and Biomechanics, Zoological Institute, Kiel University, Am Botanischen Garten 1-9, 24098 Kiel, Germany. 4 Ket Lab, Edoardo Amaldi Foundation, Italian Space Agency, Via del Politecnico snc, 00133 Rome, Italy. 5 School of Engineering and Materials Science, Queen Mary University of London, Mile End Road, E1 4NS London, UK. Correspondence and requests for materials should be addressed to F.S. (email: fas@tf.uni-kiel.de) or to N.M.P. (email: nicola.pugno@unitn.it) or to R.A. (email: ra@tf.uni-kiel.de)