On the Effect of Block Roughness in Ogee Spillways with Flip Buckets

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Abstract: In this study, the effect of the presence of bed-block roughness in an ogee spillway on energy dissipation and jet length is investigated. A series of experimental and numerical tests were conducted using an ogee spillway with block roughness on the bed without a flip bucket and with a flip bucket at different take-off angles (32 °C and 52 °C). To model the free-flow surface, the volume-of-fluid (VOF) method and turbulence model from RNG k–ε were used. Results indicated that the numerical model is fairly capable of simulating a free-flow surface over an ogee spillway; using block roughness on the spillway chute without a bucket, relative energy dissipation increased by 15.4% compared to that in the spillway with a smooth bed, while for the spillway with 32 °C and 52 °C buckets, it increased by 9.5%. The jet length for a spillway with a flip bucket and roughened bed decreased by 8% to 58% compared to that in a smooth bed. Lastly, the relationships for the estimation of relative energy dissipation and jet length are presented.

Keywords: bed roughness; physical and numerical model; ogee spillway; energy dissipation; jet length

1. Introduction

Energy-dissipating structures (i.e., hydraulic jump stilling basins, roller buckets, ski jump buckets) are usually constructed at the end of spillway discharge channels in order to dissipate the extra energy. Specifically, flip buckets are mainly placed at the end of chute spillways and outlets of high dams in order to dissipate the energy characterizing high-velocity flows [1]. So far, various models of flip buckets, such as simple, splitter, deflector, and specific compound buckets have been built, but information about the design of compound buckets is still limited and more studies are needed [2]. Flip buckets were proposed as successful hydraulic structures in the Dordogne hydraulic projects performed in France in the middle of 1930s, and after experiments carried out by Maitre and Obolenski on jet flows in 1954 [3]. Rohne and Peterka [4] conducted a study on an improved flip bucket design for the US Bureau of Reclamation. The simplest flip bucket is represented by a cylindrical shell sector tangent to the floor of the flood conduit (chute or tunnel), as suggested in studies conducted in 1993 on the Grand Coulee dam located in Washington [4]. Joun and Hager [5] evaluated the flip buckets both in the type of a prismatic rectangular channel and a bucket having a lateral flow deflector. In their research, the scale effects in the hydraulic models, pressure distribution through the bucket, flow projectile,
shock-wave creation conditions and governing choking relations were investigated [5]. Dargahi [6] performed a numerical and experimental study on an ogee spillway using Fluent® software to simulate the flow with regular mesh. Steiner et al. [7] investigated the ski jump hydraulics in a laboratory model study related to circular bucket geometry. Kermannejad et al. [8] worked on dynamic pressure due to the impact of a ski jump out of a flip bucket downstream of a chute spillway model. Their results showed that the pressure coefficient is highly sensitive to horizontal and vertical distances from the impact location and impact angle. Zhenwei and Zhiyan [9], and Parsaie et al. [10] investigated flow characteristics over chutes and the cavitation phenomenon using computational-fluid-dynamics (CFD) approaches on a spillway’s flip bucket. Daneshfaraz and Ghaderi [11] studied the effect of a reverse arch of an ogee spillway on pressure on the spillway. Yamini et al. [12] experimentally investigated the effect of entrance flow conditions on pressure fluctuation on the bed of compound flip buckets of the Gotvand dam in Iran.

One of the ways to reduce or even omit downstream energy dissipator dimensions, is to decrease the flow energy in the chutes. This can be accomplished, for example, with the use of a barrier or baffled aprons in the bed because they dissipate more hydraulic energy than corresponding conventional chutes or spillways do. A backfill is placed over one or more rows of baffles to restore the original bed elevation. When scour or downstream channel degradation occurs, successive rows of baffles are used to prevent excessive flow acceleration [13]. The baffled chute spillway relies upon multiple rows of baffles to aid in energy dissipation, as suggested by the United States Bureau of Reclamation (USBR), which conducted extensive studies on baffle block chutes to achieve an optimal design. Kaya and Emiroglu [14] investigated the effect of stepped, wedge, T-shaped, and trapezoidal blocks at different chute bed slopes on the energy dissipation of the flow passing over this structure. Elnikhely [15] examined the effect of cylindrical blocks installed on the ramp downstream of the spillway on the dimensions of a downstream scour hole.

As can be seen from the literature, most researchers have concentrated their efforts and studies on the use of energy-dissipating structures downstream of spillways or dams. However, there is still a lack of research focused on the appendance of elements on chutes as energy dissipators. The present study conducts numerical and experimental analysis on the effect of bed blocks on an ogee spillway, considering the amount of dynamic energy dissipation of water and jet length. Experiments were performed on physical models in an ogee spillway (USBR standard) with and without a flip bucket, with different take-off angles, applying the block roughness on the ogee spillway bed at a different range of Froude numbers.

2. Methods

2.1. Energy-Dissipation Analysis

The first step to develop a correlation is to select parameters that influence flow energy dissipation. In this research, we focused on the input parameters to keep correlation as simple as possible. In order to reach the aims of the present study, energy dissipation can be written as a function of the listed parameters in Equation (1):

\[
\frac{\Delta E}{E_0} = f(H_{\text{dam}}, \rho, \mu, g, V, y, R, \theta, \sigma, a),
\]

where \(\Delta E/E_0\) is the relative energy dissipation, \(H_{\text{dam}}\) is the dam height, \(\rho\) is the water density, \(\mu\) is the dynamic viscosity of water, \(g\) is the gravitational acceleration, \(V\) the approaching flow velocity, \(y\) the flow depth, \(R\) the bucket’s radius, \(\theta\) the take-off angle, \(\sigma\) the surface tension, and \(a\) the dimension of the roughness block. According to the Buckingham \(\pi\) theorem, the general relationship below can be obtained:

\[
\frac{\Delta E}{E_0} = f\left(\frac{R}{a}, \frac{y}{a}, \frac{y_e}{H_{\text{dam}}}, Fr, Re, We, \theta\right),
\]
where \( Ra \) is the relative buckets radius, \( y/a \) is the relative depth of the approach flow, \( yc/H_{dam} \) is the relative critical flow depth, \( Fr \) is the approach flow Froude number to the bucket, \( We \) is the Weber number, and \( Re \) is the Reynolds number of the flow approaching the bucket, assuming the same value in all experiments \( (Re > 1 \times 10^5) \), thus not influencing Equation (2) \[16\]. Moreover, the effect of surface tension can be neglected: when flow depth on the spillway was more than 0.05 m (in the experiments, the least flow depth on the spillway was 0.053 m), inertia force dominated, and the effects of the Weber number \( (We = \rho V^2 l / a) \) could be neglected. In this research, longitudinal dimension and roughness height \( a \) were fixed. Thus, the final equation can be summarized as:

\[
\frac{\Delta E}{E_0} = f\left( \frac{R}{a}, \frac{y}{a}, \frac{yc}{H_{dam}}, Fr, \theta \right).
\]

### 2.2. Multiphase (Water/Air) Hydraulic Model

The most common application of CFD for this area is associated with the simulation of free surfaces: open channel flows, overflows, and hydraulic jumps. The FLOW-3D® computational package, able to solve complex fluid dynamic problems, was used. This software shows high performance in modeling unsteady free-surface flows: it utilizes the finite-volume method for structured meshes to solve the three-dimensional Reynolds-averaged Navier–Stokes equations of fluid motion. These equations can be written in a Cartesian coordinate system \((x, y, z)\) as follows \[17,18\]:

\[
V_F \frac{\partial \rho}{\partial t} + \frac{\partial (\rho u A_x)}{\partial x} + \frac{\partial (\rho v A_y)}{\partial y} + \frac{\partial (\rho w A_z)}{\partial z} = R_{SOR}
\]

\[
\frac{\partial u}{\partial t} + \frac{1}{V_F} \left( u A_x \frac{\partial u}{\partial x} + v A_y \frac{\partial u}{\partial y} + w A_z \frac{\partial u}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial x} + G_x + f_x
\]

\[
\frac{\partial v}{\partial t} + \frac{1}{V_F} \left( u A_x \frac{\partial v}{\partial x} + v A_y \frac{\partial v}{\partial y} + w A_z \frac{\partial v}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial y} + G_y + f_y
\]

\[
\frac{\partial w}{\partial t} + \frac{1}{V_F} \left( u A_x \frac{\partial w}{\partial x} + v A_y \frac{\partial w}{\partial y} + w A_z \frac{\partial w}{\partial z} \right) = -\frac{1}{\rho} \frac{\partial P}{\partial z} + G_z + f_z
\]

where \((u, v, w)\) are velocity components, \(A\) symbols are the cross-sectional area of the flow associated with the flow direction, \(G\) terms are local fluid accelerations, and \(f\) terms are related to frictional forces in the respective directions; \(\rho\) indicates fluid density, \(K\) the local pressure, \(V_F\) the fractional area open to flow in the fractional area/volume obstacle representation (FAVOR) method, \(P\) the pressure, and \(R\) the source term.

A turbulence model is necessary to account for turbulent Reynolds stresses. Here, the \(k-\varepsilon\) re-normalization group (RNG) turbulence model was selected \[19,20\]. This model was applied to similar flow scenarios and is capable of providing accurate and efficient solutions \[21–27\]. The RNG \(k-\varepsilon\) model is a two-equation model expressed as:

\[
\frac{\partial}{\partial t} (\rho k) + \frac{\partial (\rho ku_i)}{\partial x_i} = \frac{\partial}{\partial x_j} \left( \alpha_k \mu_{eff} \frac{\partial k}{\partial x_j} \right) + G_k + G_b - \rho \varepsilon - Y_M + S_k
\]

\[
\frac{\partial}{\partial t} (\rho \varepsilon) + \frac{\partial (\rho \varepsilon u_i)}{\partial x_i} = \frac{\partial}{\partial x_j} \left( \alpha_\varepsilon \mu_{eff} \frac{\partial \varepsilon}{\partial x_j} \right) + C_{1\varepsilon} - \frac{\varepsilon}{k} \left( G_k + G_3 \varepsilon \right) + C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} - R_\varepsilon + S_\varepsilon
\]

where \(k\) is the turbulent kinetic energy, \(\varepsilon\) is the turbulence-dissipation rate, \(G_k\) is the production of turbulent kinetic energy that arises due to mean velocity gradient, \(G_b\) is turbulent kinetic energy production from buoyancy, \(Y_M\) is the fluctuating dilation in compressible turbulence, and \(\alpha_k\) and \(\alpha_\varepsilon\) are inverse effective Prandtl numbers for turbulent kinetic energy and its dissipation, respectively \[28\].

In the above equations, \(\alpha_k = \alpha_\varepsilon = 1.39, C_{1\varepsilon} = 1.42,\) and \(C_{2\varepsilon} = 1.6\) are model constants. All constants were
explicitly derived in the RNG procedure. Terms $S_k$ and $S_\varepsilon$ are sources terms for $k$ and $\varepsilon$, respectively. In addition, $R_\varepsilon$ is a proper term of the RNG model with respect to the $k$-$\varepsilon$ one. The following equations provide details on how effective viscosity is determined, considering molecular and turbulent effects:

$$\frac{d(\rho^2 k)}{\sqrt{\varepsilon \mu_t}} = 1.72 \frac{\nu}{\sqrt{\nu^3 - 1} + C_\nu}$$  \hspace{1cm} (10)

$$v = \mu_{eff}/\mu, \ C_{\nu} = 100$$ \hspace{1cm} (11)

where $\mu_t$ is turbulence viscosity and $\mu_{eff}$ is effective viscosity.

Since the present situation contained a free-surface interface (between water and air fluids), the software used the volume-of-fluid (VOF) method [29]. This method [30] can be summarized by Equation (12):

$$\frac{\partial F}{\partial t} + \frac{1}{V_f} \left( \frac{\partial}{\partial x}(F u A_x) + \frac{\partial}{\partial y}(F v A_y) + \frac{\partial}{\partial z}(F w A_z) \right) = 0$$ \hspace{1cm} (12)

where $A$ is the average ratio of the flow area along the $x$, $y$, and $z$ directions, and $u$, $v$, and $w$ are the average velocities along $x$, $y$, and $z$. Term $F$ is the fraction function that represents the amount of fluid in each cell: it takes values of 0 for a cell that is empty of a particular fluid, and 1 for full fluid cells [31].

3. Experimental and Numerical Test Cases

3.1. Experiment Facilities

Tests were carried out at the Maragheh University Hydraulic Laboratory. A 5 m long flume with a rectangular section (0.3 m width and 0.45 m height) bed, and walls in plexiglass (to improve flow visibility and reduce friction), was adopted. With plexiglass, the influence of sidewall effects is considered to be negligible [32,33].

Flow in the flume was generated with two pumps with a maximal flow rate of 0.075 m$^3$/s, connected to two rotameters with ±2% accuracy [34,35]. To eliminate turbulence in the entrance region, a planar mesh was added. At the inlet of the flume, there was a screen that eliminated the flow turbulence, and flow slowly entered the laboratory flume; to ensure steady flow, spillway models were installed 1.5 m downstream of the inlet tank. The physical model of the ogee spillway, based on the procedure reported in USBR (1987) [36], was fabricated from dense polyethylene and located 0.7 m far from the inlet of the flume (Figure 1), with a scale of 1:33 (height of 0.27 m, length of 0.4 m, and width of 0.3 m) on the basis of the Froude similarity criterion between model and prototype. It includes the whole ogee spillway and chute, which is 0.4 m long and connected with the flip bucket at the exit. After some pre-experiments, two types of flip buckets with take-off angles $\theta = 35^\circ$ and 52 $^\circ$, and radii $R = 19$ and 12 cm, respectively, were considered. Block roughness with length and width of 1.5 cm, and height of 0.5 cm was considered in the bed of the ogee spillway.

A gauge point mounted on the flume top was used to measure upstream and downstream flow depth on the spillway. Jet length was measured with an inserted strip in both sides of the flume. To reduce the measuring error, jet length was measured by averaging both sides of the flume considering the length of the jet as the distance between the bucket end and where the water descended. In order to accurately measure flow depth, the average of three depths measured at 5 cm intervals from the walls and in the middle of the flume was used. Then, flow velocity was calculated using the continuity equation. As shown in Figure 1, relative energy dissipation was calculated from Equation (13):

$$\Delta E_r = \left(1 - \frac{E_1}{E_0}\right)$$ \hspace{1cm} (13)

where $\Delta E_r$ is the relative energy dissipation, $E_0$ is the total energy of upstream flow, and $E_1$ is the current energy in the base of the spillway. Figure 2 and Table 1 illustrate the dimensions of the ogee spillway model with the roughness block, and list the geometric and hydraulic conditions,
respectively (parameter \(a\) in Figure 2 is the dimension of the roughness block). Considering the 1:33 scale of physical model, approach flow Froude number \(Fr = \frac{V}{(gh)^{0.5}}\) was about 1.29–3.62, with Reynolds number \(Re = \frac{Vh}{\nu}\) being about \(2.07 \times 10^4–3.895 \times 10^4\), where \(\nu\) is the kinematic water viscosity, \(g\) is the gravitational acceleration, and \(V\) and \(h\) are the mean velocity and depth of approach flow, respectively.

![Schematic of the experimental setup with an ogee spillway.](image)

**Figure 1.** Schematic of the experimental setup with an ogee spillway.

### 3.2. Numerical Domain

AutoCAD® software was used to build up the geometry of the models with a stereolithography (STL) file. According to the experiment conditions, the following boundary conditions were employed:

- inlet boundary condition was set as discharge flow rate \((Q)\);
- outflow (O) boundary condition was used downstream (at a sufficiently far location to prevent boundary effects on the results);
- the bottom and side boundaries were treated as a rigid wall \((W)\), and no-slip conditions were applied at the wall boundaries;
- an atmospheric boundary condition was set to the upper boundary of the channel, which allowed for the flow to enter and leave the domain; and
- symmetry boundary condition \((S)\) was also used at the inner boundaries.

The distance between the ogee spillway and \(X_{\text{min}}\) boundary was evaluated to be \(4H_{\text{dam}} = 1.1\) m. In fact, monitoring the water-surface variations at different stations upstream of the ogee spillway revealed that 1 m was sufficient for an undisturbed approach flow to be established. Figure 3A shows the computational domain of the present study and associated boundary conditions.

The spatial domain was meshed using a structured rectangular hexahedral mesh with two different mesh blocks (see Figure 3B). This technique, i.e., a nested mesh block, was adopted from previous studies \([34,37]\) Numerical results were obtained for five different mesh sizes (T1, T2, T3, T4, and T5) for improved computational results and subsequent validation.
As listed in Table 2, a comparison between calculated and measured free-surface profiles was performed. Figure 4 shows the variation of the mean relative error as a function of the cell sizes for mean free-surface profiles at a selected point on spillway body.

![Ogee Spillway Illustration](image1)

**Figure 2.** Illustration of ogee spillway in flume, bucket, and block.

**Table 1.** Dimensions, and hydraulic experimental and numerical parameters.

| Range | $Q$ (m$^3$/s) | $y$ (cm) | $R$ (cm) | $\Theta$ (Deg) | Fr | Re |
|-------|--------------|----------|----------|----------------|----|----|
| Min   | 0.005        | 5.3      | 12       | 32             | 1.29 | 20,700 |
| Max   | 0.014        | 11.7     | 19       | 52             | 3.62 | 38,950 |
revealed that 1 m was sufficient for an undisturbed approach flow to be established. Figure 3A shows the computational domain of the present study and associated boundary conditions.

Figure 3. Sketch of boundary conditions and mesh setup on numerical domain in FLOW-3D.

Table 2. Mesh-sensitivity analysis for present study.

| Test No. | Coarser Cell Size (cm) | Finer Cell Size (cm) | Total Mesh Number | MAPE (%) * | ** RMSE (cm) |
|----------|------------------------|----------------------|-------------------|------------|-------------|
| T1       | 1.2                    | 0.55                 | 944,125           | 19.24      | 4.6         |
| T2       | 1.1                    | 0.50                 | 1,335,000         | 8.89       | 1.94        |
| T3       | 0.95                   | 0.45                 | 1,769,834         | 8.45       | 1.75        |
| T4       | 0.80                   | 0.40                 | 2,541,311         | 2.42       | 0.39        |
| T5       | 0.70                   | 0.35                 | 3,906,163         | 1.90       | 0.33        |

* Mean absolute percentage error; $X_{\text{exp}}$: experimental value of $X$; $X_{\text{num}}$: numerical value of $X$; $n$: data count.

** Root mean square error; $X_{\text{exp}}$: experimental value of $X$; $X_{\text{num}}$: numerical value of $X$; $n$: data count.
The error between data obtained from FLOW-3D® software and experimental results was calculated according to Equation (14):

\[ E = \left| \frac{F_{SE(Exp)} - F_{SE(Num)}}{F_{SE(Exp)}} \right| \times 100 \]  

where \( E(\%) \) is the relative error percentage, \( F_{SE(Exp)} \) is the experimental free-surface elevation, and \( F_{SE(Num)} \) is the numerical counterpart. Figure 5 and Table 3 show free-surface profiles and errors. Good agreement was found between numerical and experimental data, and both of them represent a similar trend. The maximal difference between the data was related to \( X = 0.25 \) m and is equal to \( \sim 7\% \), and the overall mean values of the relative errors was \( \sim 2\% \), which confirmed the ability of the numerical model to predict flow specifications over the ogee spillway. A summary of the overall mean values of the relative errors generated for other discharges is shown in Table 4.

Figure 5. Comparison of free-surface profiles from FLOW-3D software with laboratory data; \( Q = 0.0085 \) m\(^3\)/s.
Table 3. Comparison of numerical and experimental free-surface profiles; $Q = 0.085 \text{ m}^3/\text{s}$.

| $X(\text{m})$ | $F_{SE}(\text{m})_{\text{Exp}}$ | $F_{SE}(\text{m})_{\text{Num}}$ | Relative Errors (%) | RMSE (cm) |
|---------------|-------------------------------|-------------------------------|---------------------|-----------|
| $-0.28$       | $0.326$                       | $0.330$                       | $1.22$              | $0.04$    |
| $-0.20$       | $0.327$                       | $0.331$                       | $1.22$              | $0.04$    |
| $-0.15$       | $0.325$                       | $0.330$                       | $1.53$              | $0.05$    |
| $-0.10$       | $0.324$                       | $0.328$                       | $1.22$              | $0.04$    |
| $-0.05$       | $0.324$                       | $0.325$                       | $0.38$              | $0.01$    |
| $0.00$        | $0.322$                       | $0.323$                       | $0.38$              | $0.01$    |
| $0.05$        | $0.309$                       | $0.313$                       | $1.22$              | $0.04$    |
| $0.15$        | $0.217$                       | $0.223$                       | $2.76$              | $0.06$    |
| $0.25$        | $0.116$                       | $0.124$                       | $6.89$              | $0.08$    |
| $0.35$        | $0.074$                       | $0.076$                       | $2.07$              | $0.02$    |
| $0.45$        | $0.083$                       | $0.088$                       | $1.53$              | $0.05$    |
| $0.55$        | $0.133$                       | $0.139$                       | $2.76$              | $0.06$    |
| $0.60$        | $0.144$                       | $0.148$                       | $1.22$              | $0.04$    |
| $0.65$        | $0.146$                       | $0.149$                       | $2.03$              | $0.03$    |
| Mean          |                               |                               | $1.88$              | $0.04$    |

Table 4. Summary of overall mean values of relative errors between numerical and experiment data.

| $Q(\text{m}^3/\text{s})$ | Mean Relative Errors (%) | Mean RMSE(cm) |
|--------------------------|---------------------------|---------------|
| $0.005$                  | $1.42$                    | $0.02$        |
| $0.007$                  | $1.21$                    | $0.04$        |
| $0.0085$                 | $1.88$                    | $0.04$        |
| $0.010$                  | $1.56$                    | $0.03$        |
| $0.011$                  | $1.42$                    | $0.04$        |
| $0.013$                  | $1.26$                    | $0.03$        |
| $0.014$                  | $1.47$                    | $0.04$        |

4.2. Flow Pattern Downstream of Ogee Spillway with Block Bed and Different Buckets

Figure 6 shows streamlines on the $x$–$y$ plane in the main channel (m/s) for three conditions: without buckets (A), with $\theta = 32^\circ$ buckets (B), and with $\theta = 52^\circ$ buckets (C).

The secondary current area, downstream of the chute in the “without bucket” scenario, was smaller than the ones in the “with flip bucket” scenarios for different take-off angles. In the flip bucket with $\theta = 32^\circ$ an asymmetric secondary current was formed with a larger area; in the $52^\circ$ one, it returned to the symmetry state in the plan. According to Figure 7, with the block on the chute of the ogee spillway, the area of the secondary vortices decreased, and the area of the secondary vortices disappeared.
Bary vortices decreased, and the area of the secondary vortices decreased. The secondary current area, downstream of the chute in the "without bucket" scenario, was smaller than the ones in the "with flip bucket" scenarios for different take-off angles of 32 and 52 degrees (smooth and blocked), and without a bucket for the substrate (smooth and rough).

Table 5 shows the relative values of energy dissipation for the smooth and blocked beds from the FLOW-3D results.

| Scenario Description | Mean Relative Errors (%) |
|----------------------|--------------------------|
| Without buckets (A)  | 0.05                     |
| With θ = 32° (B)     | 0.06                     |
| With θ = 52° (C)     | 0.07                     |

Figure 6. Streamlines on x–y plane. (A) Without buckets; (B) buckets with θ = 32°; (C) buckets with θ = 52°.

Figure 7. Streamlines on x–y plane. (A) Without buckets and smooth bed; (B) without buckets and block bed.

4.3. Energy Dissipation in Ogee Spillway with Block Bed and Different Buckets

To investigate the effect of the block in the ogee-spillway bed on relative energy dissipation, experiments and simulation were performed at various Froude numbers for a flip bucket with take-off angles of 32 and 52 degrees (smooth and blocked), and without a bucket for the substrate (smooth and rough).
rough). Table 5 shows the relative values of energy dissipation for the smooth and blocked beds from the FLOW-3D results.

**Table 5.** Relative energy-dissipation values for smooth and blocked bed (FLOW-3D results).

| Take-Off Angles (θ) | Bed           | Q (m³/s) | 0.005 | 0.007 | 0.0085 | 0.010 | 0.011 | 0.013 | 0.014 |
|--------------------|---------------|----------|-------|-------|--------|-------|-------|-------|-------|
|                    | Without flip bucket | Smooth   | 0.66  | 0.61  | 0.59   | 0.59  | 0.58  | 0.57  | 0.54  |
|                    |                | Blocked  | 0.78  | 0.72  | 0.67   | 0.65  | 0.64  | 0.61  | 0.58  |
| 32°                | Smooth         | 0.75    | 0.70  | 0.67   | 0.66  | 0.66  | 0.61  | 0.58  |
|                    | Blocked        | 0.81    | 0.78  | 0.75   | 0.71  | 0.69  | 0.65  | 0.64  |
| 52°                | Smooth         | 0.83    | 0.79  | 0.74   | 0.73  | 0.71  | 0.68  | 0.65  |
|                    | Blocked        | 0.83    | 0.81  | 0.78   | 0.76  | 0.75  | 0.71  | 0.69  |

The difference in the relative percentage of energy dissipation in the two previous states (smooth and blocked) was in the range of 6.8—15.4% for the ogee spillway without a bucket, and in the range of 7.4—9.37% for the ogee spillway with a flip bucket with a take-off angle of 32 degrees. For a take-off angle of 52 degrees, the difference was about 5.8%; the decrease in energy depreciation could be due to the submergence of the blocks. Figure 8 shows the effect of the block in the ogee-spillway bed for different states (with and without flip buckets) on energy dissipation.

![Block bed](image)

**Figure 8.** Difference in relative energy dissipation versus Froude number in block bed with different take-off angles.

The increase in bucket take-off angle led to a rise in relative energy dissipation. In fact, as the bucket take-off angle increased, the flow direction changed to be more upward, causing more dispersion in the air and consequently more energy dissipation. By increasing the discharge (and consequently flow depth) in all three states, relative energy dissipation was also decreased because flow resistance was reduced. Figure 9 shows the block-bed difference between smooth beds for different states (with and without flip buckets) on energy dissipation from the experimental results.
Figure 9. Difference in relative energy dissipation in smooth and block beds. (A) Without bucket; (B) bucket with \( \theta = 32^\circ \) (C) bucket with \( \theta = 52^\circ \).

According to Figure 8, by increasing the Froude numbers in different buckets, relative energy dissipation decreased in all cases, even if the relative energy dissipation ratio was larger than that of the conventional model (ogee spillway without block). Figure 10 shows the difference in energy dissipation (flow turbulence) in the state with and without blocks in the spillway bed. It was carefully observed on colorimetric meters that the block in the ogee spillway bed increased the energy dissipation of the flow in comparison with that in the conventional model in the same take-off angle buckets.

Figure 10. Comparison of flow turbulence on ogee-spillway chute with and without block bed.
4.4. Jet Length in Ogee Spillway with Block Bed and Different Buckets

In this research, with the constant assumption of other parameters, the effects of the take-off angles, the block of spillway bed, and the downstream Froude number (outlet bucket discharge) on jet length were studied. Table 6 shows the jet length for smooth and blocked beds from the FLOW-3D results.

Table 6. Jet-length values for smooth and block beds (cm; FLOW-3D results).

| Take-Off Angles (θ) | Bed    | Q (m³/s) 0.005 | Q (m³/s) 0.0070 | Q (m³/s) 0.0085 | Q (m³/s) 0.010 | Q (m³/s) 0.011 | Q (m³/s) 0.013 | Q (m³/s) 0.014 |
|---------------------|--------|---------------|----------------|----------------|---------------|---------------|---------------|---------------|
| L                   | Smooth | 20.5          | 24.5           | 29.5           | 32.7          | 37.7          | 40.3          | 42.8          |
|                     | Blocked| 8.6           | 14.0           | 20.5           | 32.0          | 32.0          | 35.9          | 39.5          |
| L                   | Smooth | 12.4          | 15.5           | 19.2           | 31.0          | 31.0          | 38.5          | 43.0          |
|                     | Blocked| 7.4           | 12.5           | 15.5           | 23.5          | 23.5          | 30.7          | 36.0          |

Figure 11 shows the variations in jet length (L) vs. Froude number (Fr) relative to discharge in a bucket with different take-off angles from the experimental results.

Figure 11. Difference in jet length versus Froude number in flip bucket with different take-off angles.

The jet length in the initial Froude number is the same for both buckets because of the low flow velocity. By increasing the Froude number, the jet length for the bucket with a 32° take-off angle was higher than that for the 52° take-off angle. In general, the length of the jets for a rough bed with a block was decreased from 8% to 58% relative to the smooth bed. With the increase in Froude number, the length of the jets was increased for both buckets. Figure 12 shows a comparison in jet lengths in the smooth- and blocked-bed cases (experiment results) at different Froude numbers. The length of the jet in the rough bed with blocks was lower than that for the smooth bed for both the 32° and 52° take-off angles. In a bucket with the take-off angle of 32 degrees, at lower discharges (lower Froude numbers), the difference between the jet length for the rough bed with a block and the smooth bed was more significant, and the rough bed with blocks had more of an impact on the length of the jet. For the flip bucket with a take-off angle of 52 degrees, in lower Froude numbers, the difference in the jet length between the smooth bed and the rough bed with block was due to the greater take-off angles.
Equations (15) and (16) allow for the prediction of relative energy dissipation and jet length. Equations were developed on the basis of the 70–30% rule for experimental and numerical results. In this method, 70% of the data were used to train the coefficients, and the remaining 30% were used to test correlation accuracy:

\[
\Delta E_r = 0.456 - 4.72 \frac{y_c}{H_{dam}} + 1.2 \frac{y_b}{B} - 0.075 \tan \theta 
\]

\[
L_r = 8971 \frac{y_c}{H_{dam}} - 79.6 \tan \theta - 22.73 
\]

where \( \Delta E_r \) and \( L_r \) are relative energy dissipation and jet length, respectively; \( \frac{y_c}{H_{dam}} \) the ratio of critical depth to dam height; \( \frac{y_b}{B} \) the ratio of bucket height to bucket width; and \( \theta \) is the take-off angles. In Figure 13, the calculated energy dissipation and jet length are compared with the experimental data (horizontal axis), and the energy-dissipation and jet-length values obtained from Equations (15) and (16) (vertical axis). The quality of this fit in energy dissipation and jet length was quantified by \( R^2 = 0.95 \) via ±7% relative error and \( R^2 = 0.96 \) via ±7.4% relative error, respectively. A scatter of points relative to the linear regression indicated that the experimental and computational values were in good agreement.

5. Discussion

This study focused on comparing experiments and a numerical model of ogee spillways with flip buckets. Although there are many studies on energy-dissipating structures downstream of spillways or dams, few works have focused on the effects of elements placed in the chute. This research contributes...
to basic knowledges regarding these dissipating structures. To this aim, two different structures were experimentally investigated and compared with the numerical results of CFD commercial software. Generally, there was good accordance between numerical and experimental data (maximal relative error in free-surface profiles was ~7%). Secondary current areas downstream of the chute were present in both scenarios, with and without flip buckets: the presence of flip buckets at different take-off angles led to an increase in secondary vortex area. With the block on the chute of the ogee spillway, the area of the secondary vortices disappeared.

Moreover, the amount of energy dissipation (compared to that in a smooth bed) increased by up to 15.4%, while jet length for the spillway was decreased by up to 58%. Starting from the experimental results, two analytical formulations were derived to investigate the amount of energy dissipation and the jet length of the ogee spillway. The proposed procedure was also used to test predictions against the experimental and numerical data, and it was highly correlated with yielding maximal errors of 7% and 7.4%, respectively.

6. Conclusions

Nowadays, flip buckets are widely used around the world because of their acceptable reliability in the field of energy depreciation. A flip bucket itself is, however, not an energy dissipator; it is an integral part of an energy-dissipation system. Flip buckets are used when energy has to be dissipated for large-velocity flows, and there is the possibility of cavitation and uplifting force in downstream structures. However, it is still an issue to investigate the cavitation between the blocked bed on the chute bed, downstream of the structure flip buckets, and the effect of a blocked bed on erosion downstream of flip buckets, caused by jet flow and a variety of shapes of blocks with the position and arrangement of block on the chute bed.

In this research, the effect of a blocked bed on an ogee-spillway chute on the amount of kinetic-energy dissipation and jet length was experimentally and numerically investigated. The numerical model was first compared with laboratory results to demonstrate the suitability of calculations for adequately capturing flow features.

Subsequently, changes to numerous independent parameters were made using a laboratory test and computational software to determine their effect on the amount of kinetic-energy dissipation and jet length. Changes included modifications to different take-off angles, bed type (smooth and rough bed), and Froude number. New correlating equations were provided for various values of the influencing parameters to allow for the prediction of the amount of energy dissipation and the jet length of the ogee spillway. The calculated results in this paper were in significantly good agreement with experimental and literature data.

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