Extending the Southern Shore of the Island of Inversion to $^{28}\text{F}$

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Detailed spectroscopy of the neutron-unbound nucleus $^{28}\text{F}$ has been performed for the first time following proton/neutron removal from $^{28}\text{Ne}/^{28}\text{F}$ beams at energies around 230 MeV/nucleon. The invariant-mass spectra were reconstructed for both the $^{27}\text{F}^*(ν)+n$ and $^{28}\text{F}^*(ν)+2n$ coincidences and revealed a series of well-defined resonances. A near-threshold state was observed in both reactions and is identified as the $^{28}\text{F}$ ground state, with $S_n(^{28}\text{F}) = -199(6)$ keV, while analysis of the $2n$ decay channel allowed a considerably improved $S_n(^{28}\text{F}) = 1620(60)$ keV to be deduced. In comparison with shell-model predictions and eikonal-model reaction calculations have allowed spin-parity assignments to be proposed for some of the lower-lying levels of $^{28}\text{F}$. Importantly, in the case of the ground state, the reconstructed $^{27}\text{F}+n$ momentum distribution following neutron removal from $^{28}\text{F}$ indicates that...
Introduction.—The study of nuclei located at the neutron dripline, beyond which they are no longer bound with respect to neutron emission, has become possible due to significant technological developments in high-intensity neutron-rich beams and high-efficiency detection arrays [1]. Despite these advances, the neutron dripline is only accessible experimentally for light nuclei ($Z \lesssim 10$) [2], and even in this region it remains a theoretical challenge to predict it [23]. Models incorporating the effect of three-nucleon forces [4, 5] have led to a better reproduction of the dripline. However, the effect of the continuum, which can drastically change the shell structure [7, 8], is not taken into account except for lighter nuclei [1]. The comparison between the isotopic chains of carbon, nitrogen and oxygen on the one hand, and of fluorine on the other, is particularly interesting: the dripline is only accessible experimentally for light nuclei (high-intensity neutron-rich beams and high-efficiency detection arrays [3]). Despite these advances, the neutron dripline is only accessible experimentally for light nuclei ($Z \lesssim 10$) [2], and even in this region it remains a theoretical challenge to predict it [23]. Models incorporating the effect of three-nucleon forces [4, 5] have led to a better reproduction of the dripline. However, the effect of the continuum, which can drastically change the shell structure [7, 8], is not taken into account except for lighter nuclei [1]. The comparison between the isotopic chains of carbon, nitrogen and oxygen on the one hand, and of fluorine on the other, is particularly interesting: the dripline is located at $N = 16$ for the former, while the fluorine chain extends to $N = 22$ ($^{31}$F [2]). The reason for this, however, is not fully understood.

In the fluorine chain, the odd neutron-number $^{28,30}$F isotopes are unbound, as they lack the extra binding energy provided by pairing. Christian et al. [10] found that $^{28}$F is unbound by 220(50) keV, and based on the agreement with the predictions of USDA/USDB shell-model calculations $^{28}$F was placed outside the “Island of Inversion” (IoI) [11]. This means that the ground state of $^{28}$F could be described by a particle-hole configuration ($\pi 0d_{5/2} \otimes \nu 0d_{5/2}^{1/2}$) with respect to an unbound core of $^{28}$O, forming a multiplet of $J^z = 1^+ - 4^+$ states in $^{26}$F [12, 13]. On the other hand, the relatively low energies of the first excited states in $^{28}$F were below the $^{26}$F gap, and the $\pi 0d_{5/2} \otimes \nu 1p_{3/2}$ coupling, should appear at low energy.

The location of the dripline in fluorine at $N = 22$ suggests a profound change in shell structure around doubly-magic $^{24}$O [15–17]. A direct experimental signature of these changes can be found in the evolution of the energies of the $3/2^+$, $7/2^-$ and $3/2^-$ states, arising from the neutron $0d_{3/2}$, $0f_{7/2}$ and $1p_{3/2}$ orbits, in the $N = 17$ isotones from $Z = 14$ to 10 (Fig. 3 of [18]). In $^{31}$Si, the spacing between the ground $3/2^+$ and the $7/2^-$ states, which is linked to the size of the $N = 20$ gap, is 3.2 MeV, and the $3/2^-$ state lies 0.5 MeV above the $7/2^-$. In $^{27}$F, the $3/2^- - 7/2^-$ gap is reduced to 2 MeV, and the $3/2^-$ level moves below the $7/2^-$ state, only 0.8 MeV above the $3/2^+$ g.s. [19, 21]. In $^{29}$Ne, the $3/2^-$ intruder state becomes the ground state [22]. This migration of levels has been suggested to be due to the hierarchy of the $p-n$ forces present above $^{24}$O [15], and in particular to the central and tensor components $^{23}$ [22].

This Letter reports on the first detailed spectroscopic study of $^{28}$F, which has been carried out using proton and neutron removal from high-energy $^{29}$Ne and $^{29}$F beams, respectively. In the former reaction, the $^{29}$Ne neutron configuration will remain unchanged and negative-parity states are expected to be populated at low energy in $^{28}$F through the removal of a $0d_{5/2}$ proton. Neutron removal, however, can lead to both positive- and negative-parity levels in $^{28}$F depending on the degree to which intruder (2$p2h$ and beyond) configurations are present in $^{29}$F. This study was possible owing to the high luminosity provided by a thick liquid H$_2$ target and the relatively intense secondary beams, coupled with state-of-the-art arrays for the detection of the high-energy neutrons and charged fragments and of the de-excitation $\gamma$-rays. The results indicate that $^{28}$F, and most probably $^{29}$F, lie within the IoI, and also suggest that $^{29}$O is not doubly magic.

Experimental setup.—The experiment was performed at the Radioactive Isotope Beam Factory (RIBF) of the RIKEN Nishina Center. Secondary beams of $^{29}$Ne ($\sim 8.1$ kHz, 228 MeV/nucleon) and $^{29}$F ($\sim 90$ Hz, 235 MeV/nucleon) were produced by fragmentation of a 345 MeV/nucleon $^{48}$Ca beam (500 pA) on a 15-mm-thick Be target, and prepared using the BigRIPS fragment separator [24–27]. Secondary beam particles were identified via their energy loss and time of flight as measured using thin plastic scintillators, and tracked on to the object point of the SAMURAI spectrometer [28] using two sets of multi-wire drift chambers, where the MINOS target [29] was located. The latter consisted of a 15cm-thick liquid-hydrogen cell surrounded by a time-projection chamber, that allowed the reconstruction of the reaction vertex with a precision of 3 mm (sigma) in the beam direction using the intersection between the trajectory of the incoming beam and the measured track(s) of the outgoing proton(s) for the $(p, pn)$ and $(p, 2p)$ reactions. The DALI2 NaI array [30] surrounded the target for the detection of the in-flight de-excitation of fragments (with an efficiency of $\varepsilon_r \sim 15\%$ at 1 MeV).

The beam-velocity reaction products were detected in the forward direction using the SAMURAI setup, including the NEBULA [31] and NeuLAND demonstrator [32] neutron arrays, placed respectively some 14 and 11 m downstream of the target. The SAMURAI superconducting dipole magnet [33], with a central field of 2.9 T and a vacuum chamber equipped with thin exit windows [34], provided for the momentum analysis of the charged fragments. Their trajectories and magnetic rigidity were de-
FIG. 1: Left: relative-energy spectra of the $^{27}$F+n system populated from the reactions (a) $^{29}$Ne(−1p) and (b) $^{29}$F(−1n). Right: same for the $^{28}$F+2n system populated from (e) $^{29}$Ne(−1p) and (f) $^{29}$F(−1n). The fit in red corresponds to a sum of resonances (blue, with the resonance energy in keV) plus a non-resonant distribution (dashed black). Center: same as left, obtained in coincidence with the 915 keV excited state of $^{27}$F (after background subtraction) populated from (c) $^{29}$Ne(−1p) and (d) $^{29}$F(−1n). The energy axis $E$ on the top right is given with respect to $S_n(^{28}$F), and orange dots mark resonances in coincidence with the corresponding fragment $\gamma$-rays (see Fig. 2).

determined using drift chambers at the entrance and exit of the magnet [28]. This information, combined with the energy loss and time of flight measured using a 24-element plastic scintillator hodoscope, provided the identification of the projectile-like fragments. The neutron momenta were derived from the time of flight, with respect to a thin plastic start detector positioned just upstream of the target, and the hit position as measured using the NEBULA and NeuLAND arrays [33], with efficiencies of $\varepsilon_n \sim 50\%$ and $\varepsilon_{nn} \sim 10\%$ for decay energies of 0–3 MeV.

Energy spectra.— The relative energy ($E_{rel}$) of the unbound $^{28}$F system was reconstructed from the momenta of the $^{26,27}$F fragments and neutron(s) [33]. The $^{28}$F+n spectra for both reactions are shown on the left of Fig. 1. The resolution is considerably improved compared to previous studies of neutron-unbound systems [10, 36], owing to the high-granularity NeuLAND array as well as the MINOS target. The resolution of $E_{rel}(^{27}$F+n) varied as $\text{FWHM} \sim 0.18 E_{rel}^{0.63}$ MeV. In order to deduce the character of resonances in $^{29}$F, the spectra were described using single-level R-matrix line-shapes [37], which were used as the input for a complete simulation of the setup (including the beam characteristics, the reaction, and the detector resolutions and acceptances), combined with a non-resonant component obtained from event-mixing [38, 39] and from the simulation of independent fragments and neutrons, respectively for the two- and three-body spectra. The results of the fit are listed on the figure and summarized in Ref. [40].

The energy spectra of Fig. 1a,b, from the $^{29}$Ne(−1p) and $^{29}$F(−1n) reactions, exhibit a lowest-lying resonance with a width of $\Gamma = 180(40)$ keV at respectively 204(16) and 198(6) keV above threshold, without any coincident $\gamma$-ray. The weighted mean, 199(6) keV, provides therefore a determination of the g.s. energy of $^{29}$F ($S_n$). This is compatible with the less precise value of 220(50) keV from Ref. [10] using the $^{29}$Ne(−1p) reaction. As shown in Fig. 1a, we observe a second peak in the (−1p) channel at 363(17) keV, which is in coincidence with the 915(12) keV transition (inset of Fig. 1b) from the decay of the excited state of $^{27}$F [14]. As such, the resonance lies at the sum energy of 1278(21) keV above threshold. As this value matches the energy of the fourth peak at 1280(30) keV, we propose that the 1280 keV state, populated in $^{29}$Ne(−1p), decays both to the ground and first-excited states of $^{27}$F, with corresponding branching ratios of 60% and 40%. The 2810 keV resonance is also observed in coincidence with the 915 keV $\gamma$-ray. It is thus placed at an energy of 3725 keV (Fig. 2). Three other resonances identified in Fig. 1a at 940, 1840 and 3660 keV are also placed in Fig. 2.

The spectrum of Fig. 1b, obtained from $^{29}$F(−1n) displays three clear resonances, including the g.s. (see above). The resonance at 996(13) keV does not fully match the 940(20) keV observed in the (−1p) reaction. We thus propose that they correspond to two different states, as shown in Fig. 2. Given the uncertainties, the 1880(80) and 1840(30) keV resonances observed in both reactions can correspond to the same state. If we require a coincidence with the 915 keV $\gamma$-ray of
one can see in Fig. 1(d) the two resonances at 406(28) and 3180(260) keV plus an additional structure at 1200(80) keV, corresponding therefore respectively to levels at 1321, 4095 and 2115 keV (Fig. 1). Note that the 406(28) keV resonance overlaps with that at 363(17) keV, which was proposed to decay in competition with the 1280(30) keV transition in the (−1p) channel with similar intensities. However, as the fit of the (−1n) data does not allow the placement of a 1280(30) keV resonance with the required intensity, we propose that the 363(17) and 406(28) keV transitions come from the decay of different states located respectively at 1280 and 1321 keV. Finally a resonance is placed at 3980 keV.

Resonances in 28F decaying by 2n emission have been identified after applying cross-talk rejection conditions to the 20F+2n events. As can be seen in Fig. 1(e,f), the lowest-lying peak produced in both the (−1p) and (−1n) reactions has compatible energies of respectively $E_{rel} = 245(32)$ and $227(88)$ keV. The states observed in the 2n decay correspond to excitation energies of $E_{rel} + S_{n}(27F)$, when referenced to the 28F g.s., or to an excitation energy of $E_{rel} + S_{2n}(28F)$. According to AME2016 [42], the uncertainty on $S_n(27F) = 1270(410)$ keV is large, which also influences the present determination of $S_{2n}(28F)$, making the placement of the resonances very uncertain.

However, we first note that the two low-energy resonances are, as for the 1840 and 1880 keV resonances in the $^{27\text{F}}+\text{n}$ decay, produced in both reactions. Second, they have compatible intrinsic widths [10], independent of the decay mode. Third, the ratios between the 245 and 1840 keV resonances in (−1p), and the 227 and 1880 keV resonances in (−1n), are the same (∼10%). This suggests that they all originate from a single state at ∼1860 keV, that decays both by 1n and 2n emission. Excellent agreement between the 1n and 2n decay spectra is obtained using $S_n(27F) = 1620(60)$ keV and $S_{2n}(28F) = 1420(60)$ keV, the latter being deduced from the present determination of $S_n(28F)$. A summary of all the levels identified is reported in Fig. 2.

Momentum distributions.—In the (−1n) reaction, the reconstructed momentum distribution of the $^{27\text{F}}+\text{n}$ system allows the orbital angular momentum of the removed neutron to be deduced [14]. The transverse-momentum distribution corresponding to the feeding of the 28F g.s. is fitted in Fig. 3(a) with eikonal-model calculations [15,16] using a combination of $\ell = 1, 3$ components. This choice of negative-parity $\ell$ values is guided by the fact that the g.s. is also produced in the $^{29}\text{Ne}(−1\text{n})$ reaction, which, as discussed earlier, is expected to lead to negative-parity states at low $E_{rel}$. The fit, which gives a spectroscopic factor of $C^2S = 0.40(6)$, is dominated by the $\ell = 1$ component (70%), meaning that the g.s. of 28F is mainly composed of an intruder $p$-wave component.

The momentum distribution of the resonance at 406 keV, Fig. 3(b), is obtained after gating on the 915 keV $\gamma$-ray transition. It is well reproduced by a pure $\ell = 2$ component, meaning that the parity of the 1321 keV state is positive, with $C^2S = 0.012(4)$. In order to account for its highly favored 1n decay through the $1/2^+$ excited state of 27F, rather than to the $5/2^+$ g.s. despite the higher energy available, we propose that it has $J^\pi = 1^+$. Indeed, this would result in an $\ell = 0$ neutron decay to the excited state, as opposed to an $\ell = 2$ decay to the ground state. Other (higher) spin values would not account for such a unique behavior. For the resonance at 996 keV, the momentum distribution, Fig. 3(c), is very well reproduced by an admixture of $\ell = 2$ (72%) and $\ell = 0$ (28%), making it another candidate for a positive-parity state, with $C^2S = 0.30(4)$.

As for the (−1p) reaction, the four most populated states, with energies 204, 940, 1280 and 1840 keV, all display momentum distributions compatible with $\ell = 2$ proton removal from the $d_{5/2}$ orbital, with $C^2S$ of respectively 0.20(3), 0.46(7), 0.50(8) and 0.22(4), summing up to about 1.4, as compared to the maximal expected occupancy of 2 for the $d_{5/2}$ orbital in 29Ne.

Shell-model calculations.—These have been performed using the $sdpf-u$-mix interaction [14] in order to predict the energy, $J^\pi$ (Fig. 2 right) and $C^2S$ values of negative- and positive-parity states in 28F. In order to assess the sensitivity to the level scheme, the $sdpf-mu$ interaction [53] has also been used. The $sdpf-u$-mix interaction has been refined in order to reproduce the observed 3/2− and 7/2− level crossing and location of the $pf$ intruder
orbits in $^{27}$Ne, $^{29}$Mg and $^{31}$Si, and the dripline at $^{31}$F.

Both calculations predict about 15 negative- and positive-parity states below 2 MeV, demonstrating that the normal and intruder configurations in $^{28}$F are very close in energy. The first 10 states have relatively pure configurations (60–80%) mostly originating from the proton 0d$_{5/2}$ and neutron 0d$_{3/2}$ and 1p$_{3/2}$ orbits, with the exception of the 5– and 6– levels that arise from a neutron in the 0f$_{7/2}$ orbit. The π0d$_{5/2}$ ⊗ ν1p$_{3/2}$ and π0d$_{5/2}$ ⊗ ν0d$_{3/2}$ couplings lead to a multiplet of $J = 1–4$ states with negative and positive parity, respectively.

The calculations predict that four negative-parity states $J^\pi = (4, 2, 1, 3)^-$ are mainly populated in the ($-1p$) reaction with dominant $\ell = 1$ components and $C^2S$ values of 0.75, 0.44, 0.35 and 0.19, in rather good agreement with experiment. We thus think we have populated this multiplet of states. Among them, a $J^\pi = 4^-$ g.s. is predicted by both calculations, with $\Gamma$ of about 180 keV, in agreement with experiment. Using similar arguments, the 940 keV state is proposed to be $J^\pi = 2^-$. The $1^-$ level is predicted to decay both to the ground (5/2$^+$) and first-excited (1/2$^+$) states of $^{27}$F with $\ell = 1$, and could correspond to the state identified at 1280 keV. As it has the highest energy in both calculations, the 1840-keV resonance is tentatively assigned as $J^\pi = 3^-$. In the ($-1n$) reaction, the $4^-$ g.s. is calculated to be the most populated among other negative-parity states with $C^2S = 0.36$, coming mostly (90%) from an $\ell = 1$ removal, to be compared with $C^2S = 0.40(6)$, with 79% of $\ell = 1$ fraction. As for the positive-parity states, produced only in the ($-1n$) reaction, both the $sd|pf-u-mix$ interaction predicts the lowest state as $J^\pi = 3^+$ with $C^2S = 0.54$, in reasonable agreement with the 996 keV state with $C^2S = 0.30(4)$. The $1^+$ state is predicted to decay principally to the first excited state of $^{27}$F with $\ell = 0$, making the 1321 keV state a good $J^\pi = 1^+$ candidate. The calculated $C^2S$ value of the $1^+$ state, 0.31, is however much larger than experiment.

The first positive-parity states are predicted too low in energy, which could be explained by effects of the continuum (not taken into account explicitly in the present calculations) that change the effective two-body matrix elements [13, 14] and induce lingering of the $\ell = 1$ states compared to $\ell = 2$ [5]. Another feature that could be related to the effects of the continuum, discussed in Ref. [7], as an apparent reduction of pairing, is the damping of the $|S_n(N) - S_n(N + 1)|$ amplitude when approaching the dripline. While these amplitudes are correctly reproduced in lighter ($N \leq 16$) fluorine isotopes by the present calculations, our experimental $S_n(27F) - S_n(28F)$ value of 1.82(6) MeV is significantly smaller than the predicted 2.8 MeV.

Conclusions.— In summary, detailed spectroscopy of $^{28}$F has been undertaken using nucleon removal from secondary beams of $^{29}$F and $^{29}$Ne, with statistics orders of magnitude higher than the previous study and unprecedented energy resolution. This was made possible through the unique combination of a thick liquid target and state-of-the-art arrays for the detection of high-energy neutrons and charged fragments, as well as deexcitation γ-rays. They proved essential to cope with the high density of states in $^{28}$F and allowed the identification of the $1n$ and $2n$ decay modes, including transitions to bound excited states of $^{26,27}$F. In addition to making comparisons with shell-model calculations, the $^{28}$F transverse-momentum distributions following neutron removal, combined with eikonal-model calculations, allowed the $\ell$ configuration of the removed neutron to be deduced.

The $^{28}$F g.s. resonance was unambiguously identified, with $S_n(28F) = -199(6)$ keV. It has a negative parity with an $\ell = 1$ content of about 80%, which places $^{28}$F inside the IoI. Based on the comparison to shell-model calculations of the decay patterns, resonance widths and $C^2S$ values, we propose that the multiplet of $J^\pi = (1–4)^-$ states originating from the π0d$_{5/2}$ ⊗ ν1p$_{3/2}$ configuration has been identified. The first positive-parity resonance ($3^+$) is proposed at 996 keV, about 560 keV higher than shell-model predictions. A candidate for a $J^\pi = 1^+$ resonance is proposed at 1321 keV. As opposed to $^{28}$F, that has well-identified positive-parity states from $p-n$ configurations above a doubly-magic $^{24}$O core, $^{28}$F displays mixed negative- and positive-parity states, with the negative-parity states being more bound. These features strongly suggest that $N = 20$ magicity is not restored at $^{28}$O. Moreover, the single-neutron removal, including the strong $\ell = 1$ feeding of the negative-parity $^{28}$F g.s., supports the suggestion, based on mass measurements, that $^{29}$F also lies within the IoI [57].

Finally, we propose a very precise value of $S_n(27F) = 1620(60)$ keV, as compared to the tabulated value of 1270(410) keV, which combined with $S_n(28F) = -199(6)$ keV leads to a reduced oscillation in the $S_n$ values of about 35% at the dripline, as compared to shell-
model calculations. This damping in the oscillations has also been recently observed in the boron isotopic chain \[39\], suggesting that a reduced pairing force may be a generic feature of dripline nuclei.

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Supplemental Material for
“Extending the Southern Shore of the Island of Inversion to 28F”

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TABLE WITH ENERGIES AND WIDTHS

Tab. S1 contains the resonance energies and widths obtained from the fit of the 27F+n Erel spectra (Fig. 1 of the paper) populated from 29Ne(−1p) and 29F(−1n) reactions, using a non-resonant component and a set of respectively seven and six Breit-Wigner line shapes with an energy-dependent width. Tab. S2 contains the same

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information but from the fit of the $^{26}\text{F}+n+n$ spectra, using respectively five and four Breit-Wigner line shapes.

### DECAY SCHEME

The different resonances observed in this work, as well as their identified decay patterns, are displayed in Fig. S1. We were not only able to obtain a precise spectroscopy of $^{28}\text{F}$ populated from two different reactions, but also to identify the way those resonances decayed. This is essential in order to determine their structure, that is related to the different decay channels they couple to. However, it is important to keep in mind that $^{28}\text{F}$ has a known $4^+$ isomeric state at around 643 keV (see Ref. [12] of the paper). Even if populated, it would not be observed in our experiment owing to its long lifetime of about 2.2 ms. This could have an impact on our proposed level scheme, if some resonances observed in the $^{26}\text{F}+2n$ system were decaying to this isomer rather than the ground state.

### PROTON TARGET CONSIDERATIONS

The direct nucleon-removal calculations used are similar to those for reactions on light nuclear targets (see Ref. [44,45] of the paper), using the eikonal (forward scattering) and sudden (fast collision) approximations to the reaction dynamics and shell-model spectroscopic factors. For reactions on a composite light nucleus (e.g. C, Be) the complex interaction between the removed nucleon and the target means that inelastic breakup (or stripping) is the dominant removal mechanism. However, on a proton target the interaction between the struck nucleon and the proton, and the corresponding $S$-matrix, describe the nucleon-nucleon (NN) system. Since at the collision energies of interest these NN collisions are entirely elastic, the removal cross section is now determined only by the elastic breakup (or diffraction dissociation) mechanism (see Ref. [45] of the paper).

This required NN $S$-matrix for the system formed by the removed nucleon and the proton target is written $S_{jp}(b)$, with $j$ the species of the removed nucleon, $j = n, p$. The NN scattering operator, a function of the NN impact parameter $b$, is conventionally written [1]:

$$S_{jp}(b) = 1 - \Gamma_{jp}(b)$$

(1)

where $\Gamma_{jp}$, called the NN profile function, is parameterized as:

$$\Gamma_{jp}(b) = \frac{\sigma_{jp}}{2\pi}(i + \alpha_{jp})g_2(\beta_{jp}, b)$$

(2)

Here $g_2(b)$, a normalized 2D Gaussian form factor:

$$g_2(\beta, b) = \frac{1}{2\pi\beta} \exp(-b^2/2\beta)$$

(3)

approximates the finite range of the NN interactions. The $\sigma_{jp}$ are the $np$ and $pp$ total cross sections, calculated here from the Charagi and Gupta parameterization of the experimental NN data [2] at the mid-target energy. The parameters $\alpha_{jp}$, the ratios of the real to the imaginary parts of the NN forward-scattering amplitudes, are interpolated from the tabulation of Ray [3].

For the associated range parameters, $\beta_{jp}$, as in Ref. [4], we require that the total and total elastic cross sections derived from the $S_{jp}$ are equal, since the NN scattering is entirely elastic, giving:

$$\beta_{jp} = \frac{\sigma_{jp}(1 + \alpha_{jp}^2)}{16\pi}$$

(4)

The remaining dynamical input, the eikonal $S$-matrix that describes the interaction of the mass $A - 1$ reaction residue with the proton target, is computed in the optical limit (or $tp$ folding approximation) to the proton-residue optical potential with the above NN parameters. This potential and $S$-matrix includes effects of the size and asymmetry of the reaction residue through its point-neutron and proton densities, approximated using spherical Skyrme SkX Hartree-Fock (HF) calculations [2]. Such calculations have been shown to provide a very good global description of the root mean squared sizes [2] and

| $^{28}\text{Ne}(p,2p)^{28}\text{F}$ | $^{28}\text{F}(p,pn)^{28}\text{F}$ |
|---|---|
| $E_\gamma$ (keV) | $E_\gamma$ (keV) |
| $\Gamma$ (keV) | $\Gamma$ (keV) |
| $204\pm16$ | $180\pm140$ |
| $198\pm6$ | $180\pm40$ |
| $940\pm20$ | $150\pm50$ |
| $996\pm13$ | $190\pm50$ |
| $1278\pm21$ | $110\pm70$ |
| $*1321\pm31$ | $50^+_{-20}$ |
| $*1280\pm30$ | $170\pm90$ |
| $1880\pm80$ | $10^+20$ |
| $1840\pm30$ | $170\pm90$ |
| $*2115\pm81$ | $200\pm120$ |
| $3660\pm100$ | $660\pm260$ |
| $3980\pm260$ | $700\pm600$ |
| $*3725\pm370$ | $470^+_{-70}$ |
| $*4095\pm270$ | $320^+_{-70}$ |

Table S1: Energies and widths obtained from the fit of the $E_{\gamma,\text{rel}}$ spectra for the $^{27}\text{F}+n$ system populated from $^{28}\text{Ne}(-1p)$ and $^{28}\text{F}(-1n)$ reactions. Energies are given with respect to $S_{3n}(28\text{F})$. The resonances extracted from the spectra in coincidence with a $\gamma$-ray in $^{27}\text{F}$ are marked with the symbol *.

| $^{26}\text{Ne}(p,2p)^{26}\text{F}$ | $^{26}\text{F}(p,pn)^{26}\text{F}$ |
|---|---|
| $E_\gamma$ (keV) | $E_\gamma$ (keV) |
| $\Gamma$ (keV) | $\Gamma$ (keV) |
| $245\pm32$ | $130\pm98$ |
| $227\pm88$ | $6^+310$ |
| $1130\pm70$ | $960\pm30$ |
| $1422\pm89$ | $821\pm290$ |
| $1984\pm50$ | $100^+_{-10}$ |
| $2103\pm120$ | $767\pm440$ |
| $2024\pm52$ | $580\pm160$ |
| $4300\pm170$ | $2900\pm330$ |
| $*2137\pm43$ | $500\pm200$ |
| $2420\pm240$ | $980\pm490$ |

Table S2: Same as Tab. S1 but for the $^{26}\text{F}+2n$ system. Energies are given with respect to $S_{3n}(26\text{F})$. The symbol * refers here to coincidences with a $\gamma$-ray in $^{26}\text{F}$.
FIG. S1: The detailed decay scheme of the different states observed in $^{28}$F, populated from $^{29}$Ne and $^{29}$F, is shown in the top and bottom panels, respectively. The widths of the levels correspond to the uncertainty on their centroid value, while the placement of the levels marked with a filled orange circle is derived from their observed coincidence with a $\gamma$-ray in the $^{27}$F or $^{26}$F spectra from the 1$n$ or 2$n$ emission, respectively. The level scheme of $^{28}$F has been divided into two regions (left and right) for better clarity.

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