Connection between Stellar Mass Distributions within Galaxies and Quenching Since $z = 2$

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Abstract

We study the history from $z \sim 2$ to $z \sim 0$ of the stellar mass assembly of quiescent and star-forming galaxies in a spatially resolved fashion. For this purpose, we use multi-wavelength imaging data from the Hubble Space Telescope (HST) over the GOODS fields and the Sloan Digital Sky Survey (SDSS) for the local population. We present the radial stellar mass surface density profiles of galaxies with $M_*/M_\odot > 10^{10}$, corrected for mass-to-light ratio ($M_*/L$) variations, and derive the half-mass radius ($R_m$), central stellar mass surface density within 1 kpc ($\Sigma_1$) and surface density at $R_m$ ($\Sigma_m$) for star-forming and quiescent galaxies and study their evolution with redshift. At fixed stellar mass, the half-mass sizes of quiescent galaxies increase from $z \sim 2$ to $z \sim 0$ by a factor of $\sim 3-5$, whereas the half-mass sizes of star-forming galaxies increase only slightly, by a factor of $\sim 2$. The central densities $\Sigma_1$ of quiescent galaxies decline slightly (by a factor of $\lesssim 1.7$) from $z \sim 2$ to $z \sim 0$, while for star-forming galaxies $\Sigma_1$ increases with time, at fixed mass. We show that the central density $\Sigma_1$ has a tighter correlation with specific star-formation rate ($sSFR$) than $\Sigma_m$ and for all masses and redshifts galaxies with higher central density are more prone to be quenched. Reaching a high central density ($\Sigma_1 \gtrsim 10^{10} M_\odot$ kpc$^2$) seems to be a prerequisite for the cessation of star formation, though a causal link between high $\Sigma_1$ and quenching is difficult to prove and their correlation can have a different origin.

Key words: galaxies: evolution – galaxies: star formation – galaxies: structure

1. Introduction

Studying the stellar mass functions of quiescent and star-forming galaxies indicates that star-forming galaxies shut down their star formation (“quenching”) with time and increase the number of quiescent galaxies (Bundy et al. 2006; Peng et al. 2010b; Ilbert et al. 2013; Moustakas et al. 2013; Muzzin et al. 2013; Tomczak et al. 2014). Consequently, the color bimodality of the galaxies exist in the local universe and persist up to high redshifts (e.g., Strateva et al. 2001; Blanton et al. 2003; Bell et al. 2004; Williams et al. 2009). Peng et al. (2010b) proposed distinct “mass” and “environment” processes or modes of quenching for central and satellite galaxies. However, as we focus on central galaxies in this paper, we do not look at environmental quenching mechanisms. To explain this bimodality, several quenching mechanisms are proposed to prevent cooling of gas in into galaxies. These processes could, e.g., expel the gas via stellar feedback or active galactic nucleus (AGN) feedback (quasar-mode; e.g., Di Matteo et al. 2005; Springel et al. 2005; Dalla Vecchia & Schaye 2008; Ciotti et al. 2009; Vogelsberger et al. 2014) or prevent cooling of the gas in the halo and keep the gas hot against further accretion to the galaxies, e.g., halo quenching (Birnboim & Dekel 2003; Kereš et al. 2005; Dekel & Birnboim 2006), AGN radio-mode feedback (Croton et al. 2006) and gravitational heating (Birnboim & Dekel 2011). Morphological quenching (Martig et al. 2009), which stabilizes the disk against gravitational collapse of gas and prevents the formation of giant molecular clouds is another recently suggested mechanism.

In addition, diverse morphologies of galaxies seen in the local universe have raised questions of how and when the galaxies assembled their stellar masses and structural components. Distinct properties of galaxies at high redshifts ($z \gtrsim 1$) compared to the local universe, indicates that galaxies of various types have gone through complex processes. Star-forming galaxies in the local universe could have consist bulges (classical, pseudo-, or peanut/boxy types), or bars in addition to the disk components. Processes that form these structural components of star-forming galaxies are still a matter of debate. Many processes, including accretion of cold gas and formation/migration of giant gas clumps, major mergers, or secular evolutionary mechanisms such as bar-instability are proposed for the formation of the galaxies central over densities or bulges (Kormendy & Kennicutt 2004; Debattista et al. 2006; Genzel et al. 2006, 2008; Carollo et al. 2007; Elmegreen et al. 2008; Dekel et al. 2009; Förster Schreiber et al. 2011; Sales et al. 2012; see also Bournaud 2016; Brooks & Christensen 2016; Fisher & Drory 2016; Kormendy 2016 for recent reviews).

Quiescent galaxies, on the other hand, are observed to have more concentrated light/mass profiles (e.g., Driver et al. 2006; Bell 2008; Bell et al. 2012) and have grown in size since $z \sim 2-3$, in particular, the average size of the population of massive quiescent galaxies has grown by a factor of three to five since the redshift of $z \approx 2$ to the present (e.g., Daddi et al. 2005; Trujillo et al. 2007; Cimatti et al. 2008; van Dokkum et al. 2008), implying that these galaxies could have assembled their stellar masses via different mechanism at different epochs. One possible channel could be the formation of compact spheroids (or “blue nuggets”) at high redshifts (Barro et al. 2013, 2014; van Dokkum et al. 2015) and their evolution at later times via other processes such as major/minor mergers (e.g., Bell et al. 2006; Khochfar &
Silk 2006; Bezanson et al. 2009; Naab et al. 2009; van Dokkum et al. 2010; Newman et al. 2012; Oser et al. 2012; Hilz et al. 2013). Considering the increasing number density of quiescent galaxies by a factor of 10 since $z \sim 2$ from studying the stellar mass functions, an alternative channel would be due to the progenitor bias, i.e., newly quenched galaxies increase the average size of the quiescent population (Carollo et al. 2013; Cassata et al. 2013; Poggianti et al. 2013; Bell et al. 2015). An open question is how much quiescent galaxies grow individually in size (e.g., by merging) and how much of the average size-increase of the population can be explained by progenitor bias. Therefore, to understand the growth of quiescent galaxies, one has to study the growth of star-forming galaxies.

The emergence of spheroidal-dominant morphology of quiescent galaxies—while they migrate from the blue cloud to the red sequence—encourages the investigation of the correlation between structural parameters with the cessation of star-formation activity. Early studies by Kauffmann et al. (2003b) demonstrate that stellar mass surface density of galaxies are better correlated with the age of galaxies than stellar mass, in the local universe (also Kauffmann et al. 2006) using the Sloan Digital Sky Survey (SDSS). The later works shows that galaxies with prominent bulges (higher Séréic index n) are more prone to be quenched (Allen et al. 2006; Driver et al. 2006; Schiminovich et al. 2007; Bell 2008; Mendez et al. 2011), implying that there might be a link between the star-formation activity and the stellar mass distribution within galaxies. Franx et al. (2008) extended this study to high redshifts and demonstrate the better correlation of the specific star-formation rate with surface density and inferred velocity dispersion than stellar mass up to $z \sim 3$ (also Mosleh et al. 2011; Wuyts et al. 2011; Bell et al. 2012; Omand et al. 2014).

Wake et al. (2012) explored SDSS galaxies and showed that central velocity dispersion is the best indicator for predicting galaxy colors than stellar mass, surface density, and Séréic index. Moreover, Cheung et al. (2012) used central stellar mass surface density ($\Sigma_1$), which is the stellar mass in the central 1 kpc region of galaxies and found that this parameter shows a less scattered relation with galaxy color than surface density, stellar mass, and Séréic index at intermediate redshift $z \sim 0.65$. Following that, Fang et al. (2013) demonstrated this for local galaxies and stated the necessity of bulge formation for galaxies to be quenched, but not sufficient. In addition, they discuss that central velocity dispersion with 1 kpc is also correlated with $\Sigma_1$ and could be a good predictor if measured robustly. Woo et al. (2015) explored the formation of compact central density for central and satellite galaxies and their halo mass dependence, and argued on the fast quenching conditions related to central density compactness compare to the slow mechanism of halos for central galaxies. Nevertheless, results of these works suggest that determining distribution of stellar masses within galaxies, in particular, central mass density, is important for a better understanding of the quenching mechanism. Though the good correlation between central mass density and quenching does not prove the causal relation, Lilly & Carollo (2016) have shown that a mass-dependent quenching mechanism acting on star-forming galaxies whose sizes follow the observed size–mass evolution leads automatically to a high central density at the onset of quenching, however, without any causal connection between the central density and quenching.

In this paper, we study the stellar mass distributions of intermediate to massive galaxies from $z = 2$ to $z \sim 0$, by deriving point-spread function (PSF) corrected stellar mass profiles of these galaxies consistently at low and high redshifts, and further comparing the corresponding mass distribution parameters with star-formation rates of the galaxies. Many studies used the evolution of light profiles of galaxies to constrain the primary mechanism for assembling the observed structural properties of galaxies at a given stellar mass. The optical-near-infrared light could be a good representative of stellar masses, though the existence of color-gradients at low and high redshifts (Franx et al. 1989; Peletier et al. 1990; La Barbera et al. 2005; van Dokkum et al. 2010; Gargiulo et al. 2011; Guo et al. 2011) could affect the estimation of the true complex underlying stellar population within galaxies. The origin of the color-gradient could be due to the variation of the stellar population age, dust content, and stellar metallicity. Consequently, as discussed by several authors (e.g., Fang et al. 2013; Szomoru et al. 2013; Tacchella et al. 2015b, 2015a; Carollo et al. 2016), the mass-weighted profiles of galaxies are more robust than the light-weighted profiles, while comparing different galaxy populations. Hence, the constrains on the assembly history of various galaxies can be provided by studying their mass growth on the central and outer regions, at different epochs. Therefore, tracing and constraining the plausible evolutionary models of galaxies could benefit from studying the evolution of the stellar mass distributions within them.

Several approaches are employed for deriving mass surface density of galaxies at low and high-$z$. In recent works by van Dokkum et al. (2010) and Patel et al. (2013b), the light profiles are converted to the mass profiles, without assuming mass-to-light ratio ($M_s/L$) gradients. Some authors (e.g., Zibetti et al. 2009; Fang et al. 2013; Szomoru et al. 2013; Tacchella et al. 2015a) overcome this by exploiting the empirical relation between rest-frame color and $M_s/L$, however, as pointed out by these authors, the effects of age, metallicity, and dust are not exactly the same and hence introduce scatter around the color–$M_s/L$ relation. To infer the variation of the stellar masses and stellar populations, Wuyts et al. (2012) and Hemmati et al. (2014) fitted stellar population models to the resolved two-dimensional images of the galaxies. Thanks to the high-resolution, sensitive instruments on board the Hubble Space Telescope (HST) such as Advanced Camera for Survey (ACS) and Wide Field Camera 3 (WFC3), this could be feasible out to high redshifts ($z \lesssim 2$–3). Although the lack of high-resolution mid-infrared (MIR) images could slightly limit this method, the multi-wavelength observations will allow for fitting the stellar population models to a large sample of galaxies at these redshifts. This approach is extended by Morishita et al. (2015) by converting two-dimensional images to one-dimensional images and median-stacking the sample of galaxies at each redshift bin prior to the spectral energy distribution (SED) modeling. The derived stellar surface density is then deconvolved to reduce the effect of PSF. Recently, Barro et al. (2015) used observed 1D profiles of galaxies to derive their mass profiles.

In this study, we exploit the SED fitting technique on one-dimensional “PSF-corrected” light profiles of individual galaxies. Instead of deriving the mass density profile from the stacked images (e.g., van Dokkum et al. 2010; Morishita et al. 2015), we derived PSF-corrected mass profiles of individual galaxies from all their available HST filters, taking into account the gradients of $M_s/L$.

The layout of this paper is as follows. In Section 2, we introduce the sample and data used in this work. The methods for deriving the stellar mass density are described in Section 3.
We present a comparison of galaxies’ mass profiles, explore the mass profile parameters on star formation activity in Sections 4 and 5, and discuss the results in Section 6. We summarize our work in Section 7. The cosmological parameters adopted in this work are $\Omega_m = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2. Data and Sample

For our analysis, we have used the catalog and imaging of the 3D-HST Treasury Program (Brammer et al. 2012; Skelton et al. 2014) on the Great Observatories Origins Deep Survey (GOODS: Giavalisco et al. 2004), GOODS-North and GOODS-South fields (GOODS-North and GOODS-South) of the Cosmic Assembly Near-IR Extragalactic Legacy Survey (CANDELS; Grogin et al. 2011; Koekemoer et al. 2011). The catalogs provided photometry, redshift (spectroscopic and photometric), and stellar mass and color of galaxies, in addition to the HST imaging of these fields, which are all available at the 3D-HST website.\(^5\) We use sources with usephot =1 (photometric quality flag) in the 3D-HST catalogs to select a reliable sample. In order to reduce the systematic effects in our methodology (described in the next section) for deriving consistent light profiles at different filters, we used PSF-matched images at different filters (smoothed to the $H_{160}$ image resolution).

In Skelton et al. (2014), the photometric redshifts are determined using the EAZY code (Brammer et al. 2008) for objects without spectroscopic redshift and the stellar masses are measured using the FAST code (Kriek et al. 2009).

The total area of GOODS-North and GOODS-South fields is about 340 arcmin$^2$. These two GOODS fields have observations on seven HST filters in common, $F435W$, $F606W$, $F775W$, $F850W$, $F125W$, $F140W$, and $F160W$ ($B_{435}, V_{606}, i_{775}, z_{850}, J_{125}, H_{140}$, and $H_{160}$, hereafter), providing sufficient wavelength coverage for deriving stellar population modeling from SED fitting, in comparison to other CANDELS fields, which have slightly shorter wavelength ranges (five filters).

\(^5\) http://3dhst.research.yale.edu/Home.html

We have divided our sample into quiescent and star-forming galaxies using UVJ color criteria (Williams et al. 2009), based on the $U - V$ and $V - J$ rest-frame colors. The EAZY code is used to derive $U - V$ and $V - J$ colors. Our criteria for selecting quiescent galaxies at $z < 2.0$, is as follows:

\begin{align*}
(U - V) > 0.88 \times (V - J) + 0.59 & \quad [0.5 < z < 2.0] \quad (1) \\
(U - V) > 0.88 \times (V - J) + 0.69 & \quad [0.0 < z < 0.5] \quad (2) \\
(U - V) > 1.3 & \quad [0.0 < z < 2.0] \quad (3)
\end{align*}

which is similar to the criteria defined by Whitaker et al. (2011). Any sources falling outside of these criteria are defined as star-forming galaxies. The combination of these equations allows separation of un-obscured and dusty star-forming galaxies from the quiescent ones, while preventing contamination. In Figure 1, we show the color criteria (solid lines) used in this study to separate star-forming and quiescent galaxies at three different redshift intervals between $0.5 \leq z \leq 2.0$. The sources are color-coded according to their total specific star formation rate from the 3D-HST catalog using the star formation rate (combined UV+IR SFR) derived by Whitaker et al. 2014 (see also Momcheva et al. 2016). As can be seen, the clumps of quiescent galaxies are clearly falling into separate regions of the UVJ diagrams. Our samples are then selected to have stellar masses $\geq 10^{10} M_\odot$. As shown by Skelton et al. (2014) and van der Wel et al. (2014), both star-forming and quiescent galaxies are complete out to the redshift of 2 (see also Morishita et al. 2015).

We have also used a sample of local galaxies using SDSS Data Release 7 (DR7) images (Abazajian et al. 2009). We randomly select 1000 galaxies at $0.06 < z < 0.08$, stellar mass matched with the total mass distributions of SDSS. The stellar masses are taken from the Max-Planck-Institute (MPA)-Johns Hopkins University (JHU) SDSS DR7 catalog (Kauffmann et al. 2003b; Salim et al. 2007) and the star-formation rate from Brinchmann et al. (2004).\(^7\) In order to divide the local sample into star-forming and quiescent, we use an analogous method to the UVJ method, using $u - r$ versus

\(^7\) http://www.mpa-garching.mpg.de/SDSS/DR7/
shorter wavelengths and depict the robustness of our size measurements. Figure 3, which shows very good consistency between the results on ellipticity, effective radius provided by 3D-methods of star-formation rate measurements.

of star-formation rate measurements. In the case in which fitting did not converge at these shorter wavelengths (or for cases with large uncertainties of the results, i.e., converging to the boundaries), we fixed the Sérisc index and \( r_e \) to the best fit of its closest longer filter. We also note that the light profiles are all circularized to remove the effects of ellipticity.

Figure 2. Quiescent and star-forming galaxies in the local universe are based on \( u-r \) color–color selection (Holden et al. 2012), analogues to high-\( z \) UVJ. Sources are color-coded according to their specific star formation rate (sSFR) from the MPA-JHU DR7 catalog (Brinchmann et al. 2004).

As shown in Figure 2, quiescent galaxies occupy a separate region from star-forming ones. Similar to Figure 1, galaxies are color-coded according to their specific SFR. We use the New York University Value-Added Galaxy Catalog (NYU-VAGC; Blanton et al. 2005) for local galaxy colors and absolute magnitudes. Note that using similar color–color selection criteria to separate quiescent and star-forming galaxies at low and high redshifts reduces biases may caused by different methods of star-formation rate measurements.

3. Methodology

3.1. Deriving Light Profiles

In this section, we describe the method for deriving the galaxies’ surface brightness profiles in all available filters. We first derive the deconvolved profiles of galaxies at different filters, which are first derived by fitting PSF convolved single Sérisc (Sérsic 1963, 1968) models to the observed two-dimensional surface brightness images of galaxies. We use GALFIT v3 (Peng et al. 2010a) to perform two-dimensional fitting, while using \( H_{160} \) band PSFs (taken from 3D-HST). The procedure is similar to that of Mosleh et al. (2012, 2013). We extract \( 48'' \times 48'' \) cutout images around each galaxy prior to the fit, and masked neighboring objects during the fitting, using the mask map provided by 3D-HST. We take initial guesses for position, ellipticity, effective radius \( r_e \), and position angle, from the original catalog and initially assumed Sérisc index of 2. We compare sizes of \( H_{160} \) band images of our galaxies for derived from our method to the ones measured by van der Wel et al. (2014, 2012), in Figure 3, which shows very good consistency between the results and depict the robustness of our size measurements.

The procedure for deriving the surface brightness profiles at shorter wavelengths (i.e., \( B_{435}, V_{606}, i_{775}, z_{850}, J_{125}, \) and \( JH_{140} \)) is similar to the \( H_{160} \) band. However, to avoid systematic errors in deriving color and stellar-mass profiles, it is essential that the light profiles in different filters originate from a common center. Hence, following La Barbera & de Carvalho (2009) and Gargiulo et al. (2011, 2012), the position, ellipticity, and position angle of the best-fit Sérisc model for \( H_{160} \) band images were adopted as priors, while fitting two-dimensional single Sérisc models to galaxy images at shorter wavelengths.

Any deviation from a single Sérisc model (due to the variation of light distributions between different bands or sub-structural components) is a matter of concern for deriving the true color and \( M_*/L \) profiles. The residual-corrected method (Szomoru et al. 2010) could help to mitigate the problem. However, this method is sensitive to the noise/background and works best for massive objects. In this study, we use a sample of galaxies in a wide range of stellar masses and, for consistency, in our analysis we only use single Sérisc model profiles. In the Appendix, we show that using the residual-corrected method should not change the overall results of this study.

The total number of objects used in this study at high-z is 2391. About 7% of sources from the original catalog have \( \leq 3 \) band detection (HST filters; in order to have sufficient wavelength coverage for deriving their mass profiles) and those with large uncertainties in their derived light profile parameters (including objects close to very bright sources) are excluded from our analysis.

The procedure for deriving light profiles of the local galaxies (\( z \sim 0 \)) is similar. We use the \( u, g, r, i, z \) images of SDSS DR7 galaxies. We use the \( r \)-band images as a reference (due to having high S/Ns) and derived the light profiles. We have used synthesized PSF images generated by the SDSS photo pipelines\(^8\) at the position of each object and for different filters, to derive the best-fit Sérisc profiles using GALFIT (see Mosleh et al. 2013, for more detail). In the following analysis, we use the circularized 1D profiles.

3.2. From Light Profile to Stellar-mass Profile

The best-model light profiles at different filters derived for each galaxy can be used to measure stellar mass, color, and

\[^8\]http://www.sdss.org/dr7/products/images/read_psf.html
mass-to-light ratio profiles. The stellar mass profile of galaxies were measured by finding the best spectral energy distribution (SED) model at each radius. We used the Fitting and Assessment of Synthesis Template (FAST) code (Kriek et al. 2009) and follow the Skelton et al. (2014) for finding the best SED models, i.e., using the Bruzual & Charlot (2003) stellar population evolution models with exponential declining star-formation history, assuming Chabrier’s (2003) initial mass function (IMF) and solar metallicity, Calzetti et al.’s (2000) dust attenuation law and allowing the $A_V$ to vary between 0 and 4.
We fixed the redshift of galaxies to the ones provided by the 3D-HST catalog. In detail, we divided the light profiles into small bins of 0.25 kpc out to 20 kpc and SED fitting each bin separately. We assigned the flux errors at each bin, which were determined using the empty aperture technique around each object in a similar way as described by Skelton et al. (2014), appropriate to the bin sizes. However, at larger radii, the model fluxes are very low, hence it is crucial to increase the (model) signal-to-noise ($S/N_{\text{model}}$) for robust SED fitting at each profile location. We used an adaptive binning method (similar to Cappellari & Copin 2003) and created bins with sufficient $S/N_{\text{model}} \gtrsim 10$ in the $J - H$ color.

The stellar masses are then measured by SED-fitting at each radius, and hence creating the stellar mass profiles of galaxies. Using $J - H$ color, which straddles age, metallicity, and dust sensitive 4000 Å and Balmer break feature and provides a better constraint on the SED modeling. We note that our test shows that the results are robust against using other colors such as $z - H$ color instead of $J - H$ or even using just the $H$-band filter.

Examples of the surface brightness profiles and stellar mass surface densities of six galaxies are shown in Figure 4. For each galaxy, the solid color lines in the upper panels, are best-fit surface brightness profiles at different filters and the dashed lines are where the surface brightness profiles of galaxies reach the average surface brightness limit of their images. The bottom panel depicts their stellar mass profiles.

For deriving the mass profiles for $z \sim 0$ galaxies, we use the iSEDfit code (Moustakas et al. 2013) and apply similar Chabrier (2003) IMF to the high-$z$ sample. We follow Kauffmann et al. (2003a) to constrain the star formation history of local galaxies, i.e., allowing a random star burst in addition to the exponential declining star formation history. Similar to the high-$z$ sample, we use $g - r$ color for adaptive binning light profiles prior to the SED fitting and deriving their mass profiles. We note that using a similar star formation history and the same code for the high-redshift object will not alter the general results of this paper, as described in the Appendices.

### 3.3. Half-mass Radius

The next step is to measure the half-mass radii from the mass profiles for each object. For that, we first interpolated between the radial mass bins and then extrapolated the mass density profiles out to 100 kpc by fitting a single Sérsic model in the outer parts of mass profiles, and then integrating the mass profiles out to this radius to find the half-mass radii. Defining the radius at which the extrapolation should be started beyond that point is not an straightforward task. In order to secure that the results were not strongly biased toward our guess of this connection point and the extrapolation process, in general, we have measured the half-mass

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**Figure 5.** Left panel: the total stellar masses derived from resolved profiles compared to the total stellar masses measured provided by the 3D-HST catalog. Right panel: simulations to show the robustness of half-mass size measurements (see the text for details). In general, there is no systematic in recovering total masses and the half-mass radii of our galaxies using the method described in this paper.

**Figure 6.** Ratio of half-mass sizes to half-light sizes vs. redshift for all quiescent (left panel) and star-forming galaxies (right panel) in our sample. At all our studied redshifts, the half-mass sizes are smaller than half-light sizes. This is also the case for star-forming and quiescent galaxies. The color points show the median of the size ratios at different redshift bins color-coded according to their stellar mass bins with their related standard errors. The ratio slightly depends on the stellar masses, i.e., for massive galaxies the half-mass to half-light size ration is smaller.
radii for each galaxy by fitting about 1000 Sérsic profiles starting at different radii and finding the most frequent output results. In order to check the reliability of this method, we applied it to a set of 3000 two-component Sérsic models of density profiles, while random noise was added to the profiles to resemble the measured mass profiles of this study. The result of our simulation shows that our method is robust and half-mass radii can be recovered without any systematic over our studied stellar mass range (bottom panel of Figure 5). The blue points in the right panel of Figure 5 are the median of the relative error of the half-mass sizes with the error on the median and average scatter of 10%. Note that our test using simulated profiles shows that fitting a single Sérsic model to entire profiles causes large scatter on derived half-mass sizes, especially for objects with $R_{\text{mm}} < 1$ kpc.

The total stellar masses derived by this method are compared to the total masses from the 3D-HST catalog in the left panel of Figure 5. There are no systematic differences between total stellar masses derived for sources using their mass density.
profiles and the ones from the original catalog. Note that we only used seven HST filters (at most) for each galaxy for SED fitting comparing to so many available complementary filters used in the 3D-HST catalog, including rest-frame near-infrared data from other instruments/telescopes. The differences in stellar mass estimates possibly arise from outshining effects or dusty regions (Zibetti et al. 2009; Maraston et al. 2010; Reddy et al. 2012; Wuyts et al. 2012; Sorba & Sawicki 2015).

Note that for the rest of the paper, we have corrected the stellar mass profile (and consequently their related parameters) to the total masses derived from the integrated star formation history using Bruzual & Charlot (2003), which includes stellar masses, remnants, and mass returned to the interstellar medium (ISM), simply, the stellar mass is the mass of gas turned into stars. The advantage of this stellar mass definition is that quiescent galaxies do not suffer from mass loss.

3.4. Half-mass versus Half-light Radius

We have compared the half-mass radii and half-light radii of our star-forming and quiescent galaxies at different redshifts and in different stellar mass bins in Figure 6. The effect of morphological K-correction has been minimized by using the half-light sizes of objects in the closest WFC3/IR or ACS band to the rest-frame ~5000 Å i.e., using H160 for sources at 1.5 < z < 2.0, J125 for objects at 1.0 < z < 1.5 and z850 for galaxies at 0.5 < z < 1.0. As shown in Figure 6, at all studied redshifts half-mass sizes are always smaller than half-light radii for both star-forming and quiescent ones (right and left panels, respectively). The color symbols represent median ratio values for different stellar mass bins. The quiescent galaxies on average have half-mass radii of about 30%-45% smaller than their half-light radii over the entire studied redshifts, which slightly depends on the stellar masses. Massive quiescent ones (10^{10.8-11.2} M_\odot) have ~45% smaller size ratios compared to the lower mass bins with ~30% size ratios. Using galaxies with >10^{10.7} M_\odot, Szomoru et al. (2013) also found smaller half-mass sizes compared to the half-light sizes but with an average of ~25% size ratios.

The ratio of sizes for star-forming galaxies, on the other hand, (right panel of Figure 6) shows little dependence on redshift. Above z > 1.5, the ratio is smaller than at lower redshifts, presumably light and stellar masses following more similar distributions; however, at lower redshifts, half-mass sizes are about 30%-50% smaller than their half-light sizes, again depending on stellar masses, with the most massive ones showing larger differences, indicating that the stellar mass profiles are more concentrated compare to their light profiles.

4. Evolution of Mass Distributions

As discussed earlier, the stellar mass distributions of galaxies at different epochs could help to study their stellar mass assembly. Therefore, in this section, we first compare the stellar mass distributions of different types (quiescent and star forming) of galaxies at different redshifts, by means of their mass profiles,
and then we study how the mass distribution varies for each type by the changes of half-mass radii and surface densities at effective radii and central compactness of our samples. We have split the sample of galaxies into four stellar mass bins for each type between $10^{10.2} - 10^{11.2} M_\odot$ and compare them at different redshifts.

### 4.1. Stellar Mass Density Profiles

The comparison of mass densities of galaxies at different epochs reveals how the distributions of stellar mass varies at fixed mass. The median radial distribution of stellar mass densities of quiescent galaxies at different redshifts are shown in Figure 7, for different mass bins (decreasing from left to right panels).

Starting from the highest stellar mass bin, i.e., quiescent galaxies within $10.8 < \log(M_*/M_\odot) < 11.2$, in the left panel, the significant changes with redshift can be seen in the outer parts of these galaxies. The density profiles of these galaxies are higher in the outer regions of these galaxies at lower redshifts compared to their high-$z$ counterparts, meaning that these galaxies have more stellar masses at their larger radii.

Clearly, it can also be seen from the middle panels of Figure 7 that intermediate massive quiescent galaxies with stellar masses of $10^{10.0} < M_*/M_\odot < 10^{10.6} M_\odot$ and $10^{10.4} < M_*/10^{10.6} M_\odot$ have similar differences in their density profiles in the outer regions at different epochs. In general, at later times, quiescent galaxies at massive and intermediate mass ranges have more assembled stellar masses at larger radii, compared to their counterparts at high-$z$. The accretion of mass via (minor) mergers or the arrival of the newly quenched systems into the red sequence, both are plausible scenarios for the differences (Naab et al. 2009; Carollo et al. 2013). This can be examined by studying the evolution of central and effective surface densities that we discuss in the following sections. It is also needed to study the evolution of the mass profiles of the star-forming galaxies.

Note that for the lowest mass bin of quiescent objects within $10^{10.2} < M_*/M_\odot < 10^{10.4} M_\odot$ (right panel of Figure 7), there is also a hint of having similar behavior, though their specific changes are small compared to the massive ones, and hence the way they change looks slightly noisy. We further test this by comparing their half-mass radii in the next section.

For the star-forming galaxies, the changes of density profiles have somewhat different behavior. Figure 8 presents the comparison of median radial density profiles at different epochs and at fixed mass bins. The most massive star-forming galaxies with stellar masses of $10.8 < \log(M_*/M_\odot) < 11.2$, have similar radial distributions of stellar masses at different redshift bins (left panel of Figure 8) with subtle changes at larger radii at later times. This shows that at any epoch, the star-forming galaxies have very similar profiles, i.e., they grow self-similar at all epochs as predicted in simulations (Tacchella et al. 2016a).

However, star-forming galaxies with intermediate stellar masses of $10^{10.2} < M_*/10^{10.6} M_\odot < 10^{10.8} M_\odot$ have different mass densities at inner and outer regions compared to their counterparts at higher redshifts. These galaxies have higher stellar mass densities within 1 kpc at later times, indicating the existence of more prominent central densities (can be expressed as bulges) at lower redshifts. Meanwhile, the stellar mass densities in the outer regions also change. Therefore, comparing low-$z$ and high-$z$ star-forming galaxies at intermediate masses, the mass densities vary at all radii, meaning that these objects have assembled stellar masses in both central and outer regions with time, with a different growth rate at the center and the outskirts. Hence it argues against the scenario of the formation of bulges prior to the disk at $z < 2$.

However, as we discuss below, central densities vary less at later times compared to the mass profiles at larger radii, therefore, suggesting slightly different timescales for their changes. Perhaps different mechanisms with different timescales could play separate roles for the evolution of mass profiles of star-forming galaxies, e.g., the accretion of gas into the disk (or maybe the bulge) and the migration of stars into the central regions via mechanisms such as disk instabilities. This needs to be addressed in more detail. Nevertheless, studying the mass profiles delineates the existence of different mechanisms of stellar mass assembly for star-forming galaxies compared to quiescent ones which is reflected into their mass distributions.

### 4.2. Half-mass Size Evolution

The evolution of the half-mass radii ($r_{\text{HM}}$) of galaxies is an effective way of illustrating their structural evolution. In the left panel of Figure 9, the evolution of median half-mass radii of quiescent galaxies between $0 < z < 2$ is illustrated for different mass bins (different colored symbols). As expected, the half-mass radii of the quiescent galaxies increases with time in a similar manner to their half-light radii (right panel of Figure 9). This is the case for galaxies at different mass bins.

We have parameterized the rate of change as a function of $(1 + z)^\epsilon$. The change of mass-weighted sizes for massive ones is as $(1 + z)^{-1.43 \pm 0.12}$. For the highest mass bin (red circles), the
half-mass sizes increase by a factor of ~4 from $z \sim 2$ to $z \sim 0$, consistent with results from the simulation by Naab et al. (2009). The half-mass size evolution is marginally faster than the evolution of their light-weighted sizes with $\alpha = -1.20 \pm 0.09$.

The pace of evolution is also similar for quiescent galaxies at lower mass bins, $\alpha = -1.56 \pm 0.13$, $-1.15 \pm 0.13$, and $-1.10 \pm 0.17$, for mass bins of $10.6 < \log(M_*/M_\odot) < 10.8$, $10.4 < \log(M_*/M_\odot) < 10.6$, and $10.2 < \log(M_*/M_\odot) < 10.4$, respectively. This shows that at fixed masses, quiescent galaxies at low redshifts have extended mass density profiles compared to their counterparts at higher redshifts.

The rate of half-mass size evolution for star-forming galaxies is not as fast as quiescent ones. The left panel of Figure 10, shows that the mass-weighted sizes of these galaxies evolve slowly for our studied mass ranges since $z \sim 2$. The rate of evolution for massive star-forming ones is $\alpha = -0.46 \pm 0.11$ slightly slower than their half-light radii evolution with $\alpha = -0.57 \pm 0.08$. The rate of half-mass size evolution is very similar for intermediate mass ranges of $10.6 < \log(M_*/M_\odot) < 10.8$ and $10.4 < \log(M_*/M_\odot) < 10.6$, with $\alpha = -0.51 \pm 0.11$ and $-0.48 \pm 0.08$, respectively. However, this is much slower for the lowest mass bin of $10.2 < \log(M_*/M_\odot) < 10.4$ with $\alpha = -0.25 \pm 0.08$, consistent with very subtle to no evolution. The slow evolution of the half-mass sizes, in combination with the results presented in Section 4.1 and Figure 8, leads us to propose two evolutionary phases of $r_m$ in star-forming galaxies, (1) self-similar changes of mass-profiles at high-$z$ (at least $z \gtrsim 1$; e.g., Tacchella et al. 2016a) and (2) increasing the disk sizes once galaxies’ central regions are saturated at later times ($z \lesssim 1$; see, e.g., Nelson et al. 2012). In detail, these trends may actually be mass dependent. It is worth noting that a flattening of the $M/L$ gradient is expected, in particular, for massive star-forming galaxies, if the effects at short rest-frame wavelengths of dust and clumpy structures are not fully taken into account. Hence, the single-Sérsic models and the methodology described in Section 3.1 could have introduced a bias affecting the rate of mass-weighted size evolution of the star-forming galaxies. However, we argue that our results do not change significantly when accounting for residuals from poor best fits (see Appendix for more details).

We note that at fixed redshift, the half-light radii of massive star-forming galaxies are larger than their less massive ones. However, the striking similarities between half-mass radii of these galaxies at different masses at fixed redshift bins, could either be representative of the similarities between the shapes of their mass profiles (having exponential shapes with different normalizations, perhaps at high-$z$) or the faster increase of the central mass densities of massive ones compared to less massive galaxies, therefore reducing the half-mass sizes for massive ones.

Overall, the changes in stellar mass-weighted radii of the star-forming galaxies is very gradual, compared to the quiescent ones at fixed mass. It has been pointed out by Lilly et al. (1998), Simard et al. (1999), Ravindranath et al. (2004), Barden et al. (2005), and van der Wel et al. (2014), that the mass–size relation of late-type galaxies has very little evolution since the redshift of $\sim 1$ (see also Dutton et al. 2011). The concurrent formation of the bulge and growth of the disk could contribute to this gradual change of half-mass sizes. Based on Tacchella et al. (2015a), the specific star formation rate (sSFR) of galaxies within $10^{10}$ and $10^{11}M_\odot$ are on average flat, which would cause very little mass-weighted size evolution. We also note that the observed rate of (light-weighted) size growth of star-forming galaxies is slightly faster: $\alpha = -0.57 \pm 0.08$ (but consistent within the errors in this study, see Figure 10). However, the exponent varies between different studies; van der Wel et al. (2014) found an observed growth of $(1+z)^{-0.75}$ for the light-weighted sizes of star-forming galaxies (see also Straatman et al. 2015). Mosleh et al. (2012) show $\alpha = -1.20$, Newman et al. (2012) observed $\alpha = -1$, and Barden et al. (2005) observed $\alpha = -0.2$. This discrepancy could first be originated from different sample selection at different redshift ranges, e.g., Barden et al. (2005) studied disk-like sample (morphological selection) at $z < 1$, while Mosleh et al. (2012) used UV-bright galaxies (color-based selection) at $z \sim 1 - 7$. In addition, different mass-normalization of the $r_c$ (i.e., different value of $\beta$ in $r_c \propto M^{\beta}$ between different studies might introduce some uncertainties. In this work, we selected star-forming galaxies based on the color–color selection method and used the $z \sim 0$ sample as a reference point for measuring the rate of (half-mass and half-light) size evolution. However, a larger sample of galaxies, in particular, between $z \sim 0$ and $z \sim 0.5$ with similar resolution are required for a better estimation of the half-mass size growth rate of star-forming galaxies. We should also mention that the accuracy of the $M/L$ gradient is particularly important for measuring the rate of half-mass size evolution. To first order, correcting the light profiles using the residual-corrected method shows that this evolution is real (Figure 25 in the Appendix illustrates this for each stellar mass bin).
Figure 13. Distributions of specific star formation rates (sSFRs) vs. central stellar mass density $\Sigma_1$ (top panels), stellar mass density at half-mass radii $\Sigma_m$ (middle panels), and average mass density within half-mass radii $\langle \Sigma_m \rangle$ (bottom rows) are shown for galaxies in our sample at different redshift bins. The galaxies are also color-coded according to their total stellar masses. It can be seen that galaxies with higher central densities have lower sSFRs at all redshifts. However, the tight "L"-shape distributions of objects on the sSFR-$\Sigma_{1\,kpc}$ plane suggest that quenching is more correlated with central densities than $\Sigma_m$ and $\langle \Sigma_m \rangle$. 

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4.3. Central and Effective Surface Density Evolution

The evolution of mass profiles can also be studied by means of the evolution of surface and central mass densities of galaxies. Stellar mass densities within the central 1 kpc region, $\Sigma_1$, is used by some authors (Cheung et al. 2012; Saracco et al. 2012; Fang et al. 2013; Tacchella et al. 2015a) as a proxy for central densities. In addition, surface density $\Sigma_m$ is another parameter that can be representative of the mass profile’s evolution. In this paper, $\Sigma_m$ is defined to be the mass surface density at the half-mass radii ($r_m$). Moreover, we also use the traditional “effective surface density,” $\langle \Sigma_m \rangle$ which is the effective surface density within half-mass radii $\left( \int_0^{r_m} 2 \pi \Sigma dr / \pi r_m^2 = M_*/2 \pi r_m^2 \right)$.

As galaxies’ half-mass sizes increase toward lower redshift, it is expected that the surface densities $\Sigma_m$ decline correspondingly. This is shown in the right panels of Figures 11 and 12, for quiescent and star-forming ones, respectively. At fixed mass, quiescent galaxies have higher surface densities in the past compared to their counterparts in the local Universe. This evolution scales as $(1+z)^{0.55 \pm 0.04}$ for massive quiescent galaxies and is similar for lower mass bins. However, the change of $\Sigma_m$ is less significant for massive star-forming galaxies with $\Sigma_m \propto (1+z)^{0.72 \pm 0.23}$ and even slower for less massive ones (see the right panel of Figure 12). The significant changes in the $\Sigma_m$ for quiescent galaxies reflects the increases of stellar masses in the outer regions, as depicted in Figure 7, implying the inside-out growth of these galaxies. For massive star-forming ones, the slow evolution of $\Sigma_m$ indicates that most of the effect is due to the mass assembly in the outer regions of low-$z$ galaxies compared to their high-$z$ counterparts. However, the marginal changes of $\Sigma_m$ for star-forming at intermediate masses is due to the increase of surface density at all radii, specifically in their central regions.

This can be further examined by the evolution of the central densities, i.e., $\Sigma_1$. In the left panel of Figure 11, the central mass density evolution of quiescent galaxies is shown at fixed masses. The central densities decline slightly and the rate of evolution is slow, $\Sigma_1 \propto (1+z)^{0.55 \pm 0.08}$ for massive quiescent galaxies, from $z \sim 2$ to $z \sim 0$. This indicates that the central regions of the massive quiescent galaxies were slightly denser at higher redshifts compared to their counterparts at low-$z$. It is worth noting that, by stellar mass, one means the time integral of the SFR. Using stellar masses of live and remnant stars will introduce more significant changes. One caveat is that this is not reflecting the true evolution of properties of individual galaxies. Overall, the slow decline of central densities might be described by the arrival of the newly quenched systems (with slightly lower $\Sigma_1$). The Lilly & Carollo (2016) model (see their Figure 12) predicts $\Sigma_1 \propto (1+z)^{0.55}$ for the evolution of the population of quiescent $\sim 10^{11}$ galaxies, which is in agreement with our findings, within the errors. Another scenario could be the possible decline in the velocity dispersion of galaxies as a result of dynamical frictions by minor mergers (Bezanson et al. 2009; Naab et al. 2009; van de Sande et al. 2013), though the contributions of mergers needs to be quantified. The $\Sigma_1$ is expected to change very slightly in the case of the inside-out scenario (Tacchella et al. 2015a). We will address this in more detail in Section 6.

For the star-forming ones, there is a weak trend of increasing $\Sigma_1$ with time up to $z \sim 0.5 \sim 1$, specifically for intermediate and less massive ones (left panel of Figure 12). $\Sigma_1$ increases from $z \sim 2$ to $z \sim 0.5$. The most massive star-forming galaxies have already reached their maximum by $z \sim 1.5$ and remain roughly constant for the redshift range of $z \sim 1.5 \sim 0.5$.

In general, assuming $\Sigma_1$ to be a bulge density, star-forming galaxies at lower redshifts have more masses in their central regions (massive bulges) compared to their analogous at high-$z$, at fixed mass. Therefore, the results above show that there should be physical processes of mass growth (as well as re-distributions of stellar masses) that increase both central and outer parts of star-forming galaxies with time.

5. Relation between Stellar Mass Densities and Quenching

As mentioned earlier, it is important to understand any relation between the stellar mass assembly of galaxies and the star formation quenching. Therefore, comparing mass profile parameters of star-forming and quiescent galaxies at different epochs is an effective way to investigate the possible relation and physical mechanisms. Several studies have already shown that galaxies with higher surface densities have lower specific star formation rates and the relation holds up to high redshifts (e.g., Kauffmann et al. 2003b; Franx et al. 2008), hence quenching seems to be correlated to the structural parameters (see also Bell et al. 2012; Bluck et al. 2014; Lang et al. 2014, and reference therein). These studies are followed by Cheung et al. (2012) and Fang et al. (2013) to show the links between quenching and bulge mass density ($\Sigma_1$) for low and intermediate redshifts. Barro et al. (2015) also investigate these relations up to $z \sim 3$. We revisit these correlations using PSF-corrected mass profiles of our sample at fixed masses in different redshift bins $0 < z < 2$ measured in a consistent way.

In Figure 13, we compare the specific star formation rate of galaxies in our sample ($>10^{10.2}M_\odot$) with surface densities within 1 kpc ($\Sigma_1$), surface densities at half-mass radii of galaxies ($\Sigma_m$) and effective surface densities within $r_m$ (i.e., $\langle \Sigma_m \rangle$). The samples are divided into four redshift bins, starting from highest redshift ($1.5 < z < 2$) in the left to the lowest redshift ($z \sim 0$) in the right panel. From the top to bottom rows, the distributions are shown for sSFR versus $\Sigma_1$, $\Sigma_m$, and $\langle \Sigma_m \rangle$, respectively, and objects are color-coded according to their total stellar masses.

As can be seen in this figure, galaxies with higher surface densities have lower sSFRs and this holds at all our studied redshifts. However, the distribution is tighter for sSFR versus $\Sigma_1$ compared to the distributions between sSFR and $\Sigma_m$ or $\langle \Sigma_m \rangle$, i.e., $\Sigma_1$ of galaxies has less scattered distribution below average sSFR of star-forming galaxies at each redshift compared to the other surface density parameters (see also Whitaker et al. 2016). The distributions of galaxies on the sSFR-$\Sigma_1$ plane is following a knee shape (or “L”-shape as already seen in Barro et al. 2015; top panels of Figure 13). This is also similar to the color-central density trend found by Fang et al. (2013).

The “L”-shape distributions of galaxies originated from two correlations, (1) the star-formation rate–stellar mass relation (SFR-M) of star-forming galaxies known as the main-sequence relation (e.g., Daddi et al. 2007; Noeske et al. 2007; Whitaker et al. 2014; Renzini & Peng 2015; Schreiber et al. 2015 and references therein) and (2) the correlation between $\Sigma_1$ and stellar masses (Saracco et al. 2012; Fang et al. 2013). The correlation between central densities ($\Sigma_1$) and stellar masses is shown to exist up to high-$z$ by several authors (Barro et al. 2015; Tacchella et al. 2015a) and also in simulations (Zolotov et al. 2015; Tacchella et al. 2016a). It is also indicated that the $\Sigma_1$-stellar mass correlation is tighter than the correlation between average surface density and total stellar masses (see Barro et al. 2015),
specifically for quiescent ones. The tighter distribution between $\Sigma_1$ and stellar masses of quiescent galaxies (low sSFRs) in comparison to their $\Sigma_m$, originated from the fact that $\Sigma_1$ of these galaxies do not change significantly, in contrast to $\Sigma_m$ which increased significantly.

Therefore, in the top panels of Figure 13, galaxies below central density thresholds, which depend on total masses and redshifts, e.g., $\Sigma_1 \lesssim 9.5 \ M_*/kpc^2$, for $1 < z < 1.5$, retain relatively constant sSFR with slight negative slopes (reflecting the main-sequence relation and the $\Sigma_1$-total mass relation). Galaxies with a critical central density threshold have left or are about to leave the main-sequence relation and the star formation is ceased in these galaxies. The distributions above $\Sigma_1$ thresholds remain less scattered by the tight correlation between $\Sigma_1$ and stellar mass of quiescent ones. It is tempting to interpret the tighter $\Sigma_1$-sSFR correlations in terms of cause and effect between central density and quenching. However, because $\Sigma_1$ also correlates with the total stellar mass, it will be difficult to say whether central density or mass drive the quenching. Therefore, the causal links are difficult to establish. We shall return to this point in Section 6.

To gain more insight on the relation between being quenched and central density, Figure 14 shows the distributions of galaxies over $\Sigma_1$ and the relative distances of galaxies to the main sequence, i.e., the $\Delta$SFR plane, for each redshift separately. We use the best-fit main-sequence relation for galaxies at high-$z$ and low-$z$ from Whitaker et al. (2014) and

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**Figure 14.** Differences between star formation rate and the main-sequence relation (at each redshifts) vs. stellar mass central densities ($\Sigma_1$). In the top rows, galaxies are color-coded according to their Sérsic indices and in the middle and bottom rows, they are color-coded according to their half-mass sizes. The gray strips represent green valley regions ($-0.8 < \Delta$ SFR $< -0.4$). The bottom row panels, show only galaxies selected as star-forming in our samples. This figure indicates that galaxies with lower SFR have more concentrated mass distributions and smaller half-mass sizes compared to those with high SFRs at all redshifts ($z < 2$).
Figure 15. Same as Figure 14, but for different stellar mass bins. At fixed mass and fixed SFR, galaxies with higher $\Sigma_1$ have smaller half-mass sizes.
Renzini & Peng (2015), respectively, to find the relative distances. Using $\Delta$SFR cancels out the redshift dependence of the distributions on SFR. Objects in the top row panels of Figure 14 are color-coded according to their Sérsic indices (form their light profiles), emphasizing previous results that objects with large distance from the main sequence have higher Sérsic indices (more concentrated; e.g., Wuyts et al. 2011).

The middle panels of Figure 14 are the same as the top panels, but are color-coded according to their half-mass sizes. This reveals that, at fixed SFR (or $\Delta$SFR), galaxies with higher central densities ($\Sigma_1$) are more compact; in other words, their stellar masses are more concentrated in their central regions. At fixed mass, this is also valid. If we split samples into four stellar mass bins (Figure 15), galaxies with higher central densities at fixed $\Delta$SFR have smaller half-mass sizes. As central densities increase, the SFR declines for star-forming galaxies. This leads to nominate $\Sigma_1$ thresholds to start the quenching mechanism at least up to $z \sim 2$.

The bottom panels of Figure 14 shows the same distributions but only for those classified as star-forming in our sample. At a fixed central mass density, there is no indication that star-forming galaxies below and above the main sequence are more (or maybe less) compact (see also Figure 15), which is consistent with the results of recent simulations (Tacchella et al. 2016b). However, these plots point out that star-forming galaxies with higher central densities have smaller mass-weighted sizes with a negative tilt between $\Delta$SFR and $\Sigma_1$.

If increasing the central mass density is correlated with quenching, then, at fixed mass, galaxies that leave the main sequence should have similar mass profiles, particularly in their central regions. To investigate this, we first split the plane of $\Sigma_1$-$\Delta$SFR into three main parallel regions, i.e., galaxies on the main sequence ($\Delta$SFR > $-$0.4), galaxies in the green valley regions ($-0.8 < \Delta$ SFR $< -0.4$), and quenched galaxies ($\Delta$SFR $< -0.8$). We compare the median mass profiles of galaxies at fixed masses of these three regions in Figures 16.
and 17, for each redshift bins, separately (left to right panels, from high-z to low-z, respectively).

In these figures, red, green, and blue lines represent the mass densities of quenched, green valley, and main-sequence galaxies, respectively. The median half-mass sizes for each profile are mentioned in each panel accordingly. As can be seen, at fixed masses, quenched galaxies have higher central densities and smaller half-mass sizes compared to the main-sequence ones. The green valley objects (recently quenched or in transition) also have higher central density profiles compared to the main-sequence ones, and their mass profiles are similar to the quenched ones, and this holds at all redshifts up to \( z \sim 2 \). The half-mass size values of green valley galaxies are in between main-sequence and quenched ones. One caveat is that, at \( z \sim 0 \), massive galaxies on the main sequence and green valley (with \( \log(M_*/M_\odot) > 10.6 \)) have similar mass density profiles, indicating that these galaxies are potentially subject to quenching.

These results seem to indicate a high central density as a prerequisite for quenching. However, Lilly & Carollo (2016) have shown that there may be no direct causality between central density and quenching because both may be driven by a third factor, such as the galaxy mass. Still, we emphasize that the relatively empty region at low \( \Sigma_1 \) and low \( \Delta \text{sSFR} \) implies that, at least for our studied mass range, almost no galaxies can be quenched prior to reaching a certain \( \Sigma_1 \) threshold, so there might always be a “compaction” phase prior to quenching. If star-forming galaxies quench after reaching a required bulge mass density, then their mass profiles should become similar to that of the quenched galaxies at later times. We will address this in the next section, in addition to the mass and redshift dependence of \( \Sigma_1 \) thresholds.

6. Discussion

The results of previous sections are useful to indicate the necessity of bulge formation before the secession of star formation, but the causality links are difficult to establish. It is possible that the “mass quenching” process (Peng et al. 2010a) alone is able to establish a density-quenching correlation, simply because the first galaxies to (mass) quench are the most dense. Still, it remains important to first understand how galaxies build up their central regions and how the mass profiles of galaxies...
change once they start quenching by reaching a certain central density limit. Second, what mechanism(s) related to the bulge growth can play a role in preventing the gas to cool and for how long? We try to address these questions in the following.

6.1. Formation and Evolution of Central Concentration

In Section 4, we have shown that at fixed mass, central mass concentration (resembling bulges) of star-forming galaxies increases with time by a factor of about two to four between \( z \sim 2 \) and \( z \sim 0.5 \) (depending on the total stellar mass). Star-forming galaxies can build and grow their bulges via different proposed mechanisms, including violent disk instabilities and mergers of giant clumps at high redshifts (e.g., Noguchi 1999; Bournaud et al. 2007; Elmegreen et al. 2008; Ceverino et al. 2010), weak disk instabilities, a.k.a., secular evolution (Kormendy & Kennicutt 2004) and inflow of gas via mergers (e.g., Fisher & Drory 2008; Hopkins et al. 2009, 2010). These processes depend on the redshift, for instance, due to the high gas fraction at high redshifts (Daddi et al. 2010; Tacconi et al. 2010), formation of giant \( 10^{8} - 9M_{\odot} \) clumps by strong gravitational instabilities and hence coalescence of them to build bulges (e.g., Genzel et al. 2011; Guo et al. 2012). However, at low-\( z \), weak instabilities of galaxies’ sub-components, such as bars, can likely trigger formation/evolution of bulges (see also recent reviews by Bournaud 2016; Brooks & Christensen 2016; Falcón-Barroso 2016; Fisher & Drory 2016; Kormendy 2016) and references therein.

For simulated galaxies Tacchella et al. (2016a, 2016b) argued that oscillations about the main-sequence ridge are important, i.e., when galaxies are above the main sequence, they form most of their stars in the bulge, while when then are below the main sequence, they form most of their stars in the disk. The outcome is that the mass in the central and outer regions grows concurrently. As shown in Figure 12, there are some hints that lower mass star-forming galaxies form their bulges at later times than massive ones, concurrently with their disk. Star-forming galaxies with moderate-mass form their bulges about 2–3 Gyr later, compared to the massive ones. Therefore, viable mechanisms might also depend on the total stellar mass of galaxies and hence the “compaction” phase (e.g., Dekel & Burkert 2014; Zolotov et al. 2015; Tacchella et al. 2016a, 2016b) can be different processes at different redshift and mass. In addition, we have also seen that at fixed mass, disks of star-forming galaxies grow with time in lockstep with bulges (van Dokkum et al. 2013; Patel et al. 2013a), hence indicating that the bulge formation mechanism(s), such as violent gas inflow induced by counter rotating streams and/or merging supported by violent disk instabilities presumably should be able to preserve the disks. Note that in this work, we have compared similarly selected galaxies at fixed masses, therefore the true evolution of individual galaxies with different stellar masses needs to be understood. Nevertheless, bulges of star-forming galaxies grow with time up to a certain value (stellar mass dependent) and possibly retain their bulge masses roughly constant thereafter.

On the other hand, at fixed mass, quiescent galaxies at \( z \sim 0 \) have slightly lower \( \Sigma_{1} \) values compared to their high-\( z \) counterparts (see Figure 11). If quiescent galaxies grow inside-out, then it is expected that \( \Sigma_{1} \) remains roughly constant, i.e., galaxies’ central densities remain almost intact after they become quenched. However, as pointed earlier, the newly quenched galaxies could introduce biases and decrease the average \( \Sigma_{1} \) values. To further examine this, it is necessary to trace back individual galaxies out to early times, which is observationally difficult. Statistically, it is proposed to use the “constant” cumulative number density approach (van Dokkum et al. 2010); however, this method fails to consider different galaxy mergers and scatter in mass accretion histories (see, e.g., Torrey et al. 2015). Marchesini et al. (2014) takes into account these effects by using the abundance matching method (Behroozi et al. 2013) and cumulative number density evolution of massive galaxies to match progenitors and descendants. If we use this later approach only for massive quiescent galaxies (Figure 18), we see little to no evolution of the central densities for quiescent galaxies ending up at \( 10^{11.2} M_{\odot} \) quiescent galaxies at \( z \sim 0 \) (i.e., \( \Sigma_{1} \propto (1 + z)^{0.27 \pm 0.12} \)). For that, we have used Baldry et al. (2008; \( z \sim 0 \)) and Tomczak et al. (2014; high-\( z \)) mass functions to estimate the cumulative number densities at different redshifts. Similar results were also found by van de Sande et al. (2013; see also Bezanson et al. 2009; Oser et al. 2012). However, this approach is still problematic because so many galaxies of different stellar masses can end up at \( z \sim 0 \) with \( > 10^{11} M_{\odot} \).
We now use a simple empirical model to interpret the observed evolution of the central density of quiescent galaxies \( (S_1^Q) \). For each pair of redshifts \( z_1 \) and \( z_2 \) (\( z_1 > z_2 \)), we write

\[
\Sigma_{l_\nu}(z_2) = \frac{n_\nu(z_1) \cdot \Sigma_Q(z_1) + (n_\nu(z_2) - n_\nu(z_1)) \cdot \Sigma_{l_\nu}(z_1)}{n_\nu(z_2)},
\]

where \( n \) is the comoving number density of galaxies in the considered mass bin. This assumes that the central density of quiescent galaxies at \( z_1 \) remains identical at \( z_2 \) and that the star-forming galaxies that quench between \( z_1 \) and \( z_2 \) maintain the central mass density they had at \( z_1 \). In this way, we model the effect of the so-called progenitor bias. We have used the number density of quiescent and star-forming galaxies at different redshifts from Tomczak et al. (2014) and the results for our higher mass bin are shown in Figure 19. The predicted central density of quiescent galaxies is shown by gray circles and compared to the observational results as in Figure 11 (red circles). The green circles also shows the observed ones but with different redshift binning (i.e., binning similar to the ones used

Figure 20. Comparing the expected \( z \sim 0 \) stellar mass profiles of star-forming galaxies at \( z \sim 0.75 \) (blue lines) with the observed local quiescent galaxies at \( z \sim 0 \) (red lines) at fixed masses (different panels, decreasing from left to right). The star-forming galaxies at these mass ranges reached their maximum central densities by \( z \sim 0.75 \). Hence, this simple test illustrates what the mass profiles of star-forming galaxies at high-\( z \) will look like once they become completely quenched by \( z \sim 0 \) (ignoring the effects of major mergers). The stellar mass profiles of these galaxies are very similar, specifically in the central regions, indicating that the transformation of star-forming galaxies to quenched objects after reaching the \( \Sigma_1 \) threshold is plausible. The solid lines are the median of profiles and shaded regions show the 1\( \sigma \) scatter.

Figure 21. Similar to Figure 20 but comparing the expected \( z \sim 0 \) stellar mass profiles of star-forming galaxies at \( z \sim 1.25 \) (higher redshift bins) with the local quiescent galaxies at \( z \sim 0 \) at fixed masses. Except for the most massive bin (left panel) in which galaxies reached to their maximum central densities, intermediate star-forming galaxies have different mass profiles, specifically in their central regions, indicating the necessity for building the central bulges.

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for the model). Any difference between the value calculated with this equation and the actual data could be ascribed to other effects, such as a structural evolution of individual galaxies. However, the predicted central densities agree quite well with the observed ones, implying that the central regions of galaxies do not evolve much following quenching.

6.2. Relation between $\Sigma_1$ and Quenching

As shown in Figures 14 and 15, at fixed mass, the star formation of galaxies declines sharply around a specific $\Sigma_1$ threshold. This can suggest a “knee-shaped” or “L-shaped” evolutionary path on sSFR-$\Sigma_1$ or color-$\Sigma_1$ planes at all our studied redshifts and different mass bins (as also suggested by Barro et al. 2015). The total stellar mass and central density of galaxies $\Sigma_1$ are correlated (e.g., Tacchella et al. 2015a). In addition, simulations show that while the total stellar masses of star-forming galaxies increase, their central densities also grow (via star formation or redistribution of stellar masses) until they saturate around a specific central density (see, e.g., Tacchella et al. 2016a). Therefore, at first sight, this may suggest that the galaxies start to quench once they reach a certain $\Sigma_1$ threshold. This looks to be the same across all our studied redshifts, though the threshold values tend slightly on the redshifts (higher values for high-$z$ galaxies). This is consistent with early observational studies on galaxies’ mass profiles at low and intermediate redshifts (Cheung et al. 2012; Fang et al. 2013), at higher redshifts (Barro et al. 2015; Tacchella et al. 2015a), and simulations (Tacchella et al. 2016a; see also Bell et al. 2012; Bluck et al. 2014; Lang et al. 2014; van Dokkum et al. 2014; Brennan et al. 2015; Teimoorinia et al. 2016; Whitaker et al. 2016). However, as mentioned earlier, the links between cause and effects are difficult to establish. We note that the advantage of this work compared to previous studies is to use PSF-corrected mass-profiles and reducing the uncertainties due to $M/L$ and color-gradients in a consistent way from $z \approx 2$ to 0.

To further understand this transition, we compare galaxy mass profiles. From Figure 12, it can be seen that at $z \approx 0.7$ star-forming galaxies (with $\log(M_*/M_\odot) > 10.4$) have already reached to their maximum central densities at fixed masses compared to their counterparts at high-$z$. Therefore, if these galaxies will become quenched at later times, then their expected mass profiles should be comparable to the quiescent ones at $z \approx 0$ with similar masses (assuming galaxies will not experience major mergers, which is less frequent at low redshifts). In other words, assuming quiescent galaxies in the local universe have once been star-forming at high redshifts and they have gradually become quenched without any significant changes in their internal structures, then it is expected that their mass distributions become comparable to the local quenched galaxies at fixed masses (the inside-out quenching scenario, see also Tacchella et al. 2016a and Onodera et al. 2015).

We put this in a simple test and investigate it by using stellar population synthesis models of Bruzual & Charlot (2003) to predict their mass profiles at $z \approx 0$ and compare them to local quiescent galaxies at fixed masses. For this purpose, we used the best-fit parameters of the star formation rate and the age derived from SED fitting, in addition to the stellar population model created with the same parameters. Using the table of the age and stellar mass from the stellar population model, the expected stellar mass at a specific time (here $z \approx 0$) is estimated. The comparison between predicted mass-profiles at $z \approx 0$ of high-$z$ star-forming galaxies ($z \approx 0.75$) are shown in Figure 20, divided into three mass bins, decreasing from left to right. For most massive bins (left and middle panels), the expected mass profiles are very similar to local quiescent ones, at all radii. For the lowest mass bin (right panel), the predicted mass profile of star-forming ones is slightly extended and less compact as the quiescent galaxies at low-$z$. Perhaps, additional process(es) is required to redistribute stellar masses or assemble masses in their central regions. Note that these less massive galaxies build their central densities later, hence using a lower redshift sample would help for this test.

In Figure 21, we show the same but for the star-forming galaxies at $z \approx 1.25$. The $z \approx 0$ expected profiles of most massive star-forming galaxies at $z \approx 1.25$ is very similar to the quiescent ones in the local Universe. These massive star-forming galaxies have reached their relative maximum central densities by $z \approx 1.5$. This shows indeed that stellar mass and central density are correlated, hence it is difficult to disentangle whether it is mass or density (or even the halo mass) that controls the quenching. However, for intermediate mass bins (middle and right panels), which have not reached their maximum central densities by $z \approx 1.25$, their expected profiles differs from the low-$z$ quiescent ones. They have more extended and less concentrated mass profiles. Note that objects in the low-mass bins might change their “mass bin” before they quench. This test recalls that star-forming galaxies at this high-$z$ need to grow their central densities and reach a specific $\Sigma_1$ threshold value prior to their quenching.

The specific threshold of $\Sigma_1$ values depends on stellar mass and redshifts. It can be defined approximately by the median values of galaxies in green valleys (gray shaded region of Figure 15) for each stellar mass and is shown in Figure 22. The specific threshold values increase with redshift at fixed mass, implying higher central density threshold requirements for galaxies at high-$z$ to become quenched. Franx et al. (2008) showed a similar evolution for the effective surface density threshold and suggested that the reason for this evolution could be due to the higher specific star formation rate at higher redshift.

It is worth noting that central density is strongly correlated with central velocity dispersion ($\sigma_1$), as derived by Fang et al. (2013) from the virial theorem. It has also been pointed out by Wake et al. (2012) that central velocity dispersion is better correlated with the color of galaxies. Therefore, $\sigma_1$-sSFR might have a similar or tighter correlation than $\Sigma_1$. This needs to be
examined observationally for a large redshift range, though it is very expensive.

7. Summary and Conclusions

In this paper, we have derived PSF-corrected stellar mass profiles of a 2391 mass-complete sample of $>10^{10} M_\odot$ galaxies up to $z \sim 2$ from 3D-HST catalog and randomly selected $\sim 1000$ mass-matched $>10^{10} M_\odot$ galaxies at $z \sim 0$. We examined the half-mass radii of star-forming and quiescent galaxies in small stellar mass bins. We also examined the relation between stellar mass structural parameters and star formation activity. We find the following.

1. Half-mass radii of all types of galaxies are on average smaller that their half-light radii (by $\sim 30\%$--$50\%$) with a weak dependence on stellar masses.

2. At fixed mass, the average half-mass size of quiescent galaxies increases by a factor of four since $z \sim 2$ in a similar pace to their half-light radii ($R_m \propto (1 + z)^{-1.43 \pm 0.12}$ for massive quiescent galaxies). Mass-weighted sizes of star-forming galaxies change very little at fixed mass ($R_m \propto (1 + z)^{-0.46 \pm 0.11}$ for massive star-forming galaxies).

3. Star-forming galaxies build up their central densities with cosmic time concurrently with their outer regions. Quiescent galaxies build up most of the stellar mass in their outskirts.

4. Stellar mass central density within 1 kpc of galaxies ($\Sigma_1$) is better correlated with sSFR than effective surface density at all studied redshift.

5. Galaxies follow a “knee-shaped” path on the $\Sigma_1$-$\Delta sSFR$ plane at all masses and are independent of redshift, i.e., galaxies need to build central densities before quenching. Threshold $\Sigma_1$ depends on redshift and stellar mass.

6. We emphasize that the correlation between $\Sigma_1$ and sSFR does not imply a causal link.

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Appendix A

Different Star Formation History

Using a different star formation history (SFH) at low and high redshift could introduce systematic effects on the derived parameters. As discussed in the text, we have assumed an exponentially declining SFH for the high-redshift sample. However, at low redshift, we assumed a stochastic burst in addition to the declining SFH, also assuming an additional burst could introduce a systematic in total stellar masses (Pozzetti et al. 2007). To examine whether our results depend on these choices, we repeat the analysis at high redshift, assuming a similar SFH at low-$z$, using the iSEDfit code. We remeasure half-mass radii using the new stellar mass profiles and show their evolution at fixed masses for quiescent and star-forming galaxies in the left and right panels of Figure 23, respectively. It can be seen that our results do not depend on the assumption of different SFHs.

Appendix B

Residual-corrected Method for Deriving Light Profiles

The complexity of the light profiles of galaxies due to sub-structural components (e.g., inner disks, clumpy features, etc.) could have introduced deviations of galaxies’ surface brightness profiles from the best-fit single-Sérsic profiles and consequently, on the derived stellar mass densities. To test whether this could have affected the results of this work, we follow Szomoru et al. (2010, 2012) and apply the same technique to derive the corrected surface brightness profiles in different filters. The deconvolved profiles of galaxies are derived by fitting PSF convolved single-Sérsic models to the observed two-dimensional surface brightness images of galaxies. We then derived the residual profile of galaxies, taking into account the geometry and position of the best-fit model and added this to the best-fit deconvolved Sérsic model. Where the uncertainties of the sky background dominate, we extrapolated the profiles at the larger radii, using a Sérsic model profile. The stellar mass surface density was then derived from these corrected surface brightness profiles in the same way as described in Section 3.2.

The right and left panels of Figure 24 show the evolution with redshift of half-mass radii of star-forming and quiescent galaxies, respectively. A comparison with the left panels of Figures 9 and 10 shows that the rate of evolution of half-mass radii of both quiescent and star-forming galaxies are consistent with the results based on the best-fit single-Sérsic models. This indicates that, independent of the method for deriving the stellar mass profiles, the half-mass radii of quiescent galaxies at fixed masses increase with time. Similarly, for the star-forming galaxies, the rate of evolution of the half-mass at fixed masses is slower than for quiescent galaxies.

In Figure 25, we show in detail the evolution of half-mass radii of star-forming galaxies using the residual-corrected method. The gray points show the mass-weighted sizes for individual galaxies and the color symbols show the medians in each redshift bin.
Figure 23. Evolution of half-mass radii of galaxies at fixed masses, assuming a different star formation history at higher redshifts, i.e., using a random burst in addition to an exponential declining star formation history. The results will not be altered by assuming a different star formation history.

Figure 24. Evolution of half-mass radii of galaxies at fixed masses, derived using the residual-corrected profile method by Szomoru et al. (2010). The rate of evolution for star-forming and quiescent galaxies at different mass bins are consistent with the results in Figures 9 and 10, assuming single Sérsic models.

Figure 25. Evolution of mass-weighted sizes of star-forming galaxies at different stellar mass bins (different panels). The gray points represents the half-mass sizes of individual galaxies and the colored circles are their medians at different redshifts. The solid lines are the best-fit size evolution to the data points. The star-forming galaxies show little size evolution at fixed masses with redshift.
The best-fit single Sérsic models are compared in 1D and 2D to the observed light profiles of a few galaxies in Figure 26. We conclude that, with the current resolution of HST images, the results of this paper are robust when using the stellar mass profiles derived from single-Sérsic models.

Figure 26. From left to right, we show the $H$-band postage stamps of a few galaxies in our sample, their best-fit single Sérsic models, the residuals, mask maps, and the comparison of 1D observed light profiles (gray lines) with their best-fit models (dashed red lines). Using single Sérsic models for galaxies in this study can recover the true properties of galaxy light profiles.
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