Quasi-one-dimensional density of states in a single quantum ring

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Generally confinement size is considered to determine the dimensionality of nanostructures. While the exciton Bohr radius is used as a criterion to define either weak or strong confinement in optical experiments, the binding energy of confined excitons is difficult to measure experimentally. One alternative is to use the temperature dependence of the radiative recombination time, which has been employed previously in quantum wells and quantum wires. A one-dimensional loop structure is often assumed to model quantum rings, but this approximation ceases to be valid when the rim width becomes comparable to the ring radius. We have evaluated the density of states in a single quantum ring by measuring the temperature dependence of the radiative recombination of excitons, where the photoluminescence decay time as a function of temperature was calibrated by using the low temperature integrated intensity and linewidth. We conclude that the quasi-continuous finely-spaced levels arising from the rotation energy give rise to a quasi-one-dimensional density of states, as long as the confined exciton is allowed to rotate around the opening of the anisotropic ring structure, which has a finite rim width.

Recently, great progress in droplet epitaxy techniques have enabled the growth of novel nanostructures1–5. In particular, semiconductor quantum rings (QRs) are of great interest as candidates for the optical Aharonov-Bohm (AB) effect6–10. As the orbital angular momentum of an electron rotating around a QR is quantized, finely-spaced energy levels appear in between the radially confined energy levels for a finite rim width. As the magnetic flux threading a QR cross section is increased, the ring orbital angular momentum of the lowest energy level as a function of external magnetic field (B) changes periodically. Therefore, oscillations in the ground state exciton emission energy with B can be observed, where the oscillation period is determined by the orbit size, rim width, and the effective mass of the electron and hole.

The morphology of QRs was observed to be different from that of an ideal ring structure, where the lateral shape ellipticity and rim height anisotropy are ignored. When a volcano-like rim anisotropy is present11–15, the wavefunction becomes localized with a crescent-like shape16–18. Provided that the degree of localization is moderate, rotational motion of an exciton around the whole circumference can be possible through tunneling. However, the condition depends on the ring morphology. As the cylindrical symmetry breaks down in the lateral structure, the orbital angular momentum no longer represents the eigenstates. In this case, the finely-spaced levels can be described by a linear combination of the quantized orbital angular momentum states, with a consequent significant modification of the selection rules. Therefore, the finely-spaced levels of a volcano-like anisotropic ring structure are different from those in a simplified ring model19–21.

According to the exciton AB oscillation of a single QR20, the level spacing and linewidth of the finely-spaced levels (~0.1 meV) were found to be comparable in a QR. In this case, a density of the these states (D(ε) ~ εν) can be defined as a function of energy (ε). The exponent (ν) can be estimated experimentally by considering the ratio of the radiative decay rate near the ground state with respect to the stochastic fraction of excitons contributing to recombination (τ ~ Γεν). This results in a temperature dependence for the radiative recombination time (τ ~ Tν). This experimental method has been used in bulk semiconductors (ν = 0.5), quantum wells (ν = 0), and quantum wires (ν = −0.5), giving rise to α = 1.5, 1, and 0.5, respectively21–23. In this work, we have investigated

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\[ E \propto \beta \text{ for a real QR in the absence of } B \text{ in terms of } \tau_r(T) \text{ and } r(T), \text{ which were obtained by using the temperature dependence of the linewidth, the time-resolved, and time-integrated photoluminescence (PL) intensities.} \]

**Results and Discussion**

As shown in Fig. 1(a), ring structures were observed in a field emission scanning electron microscope (FESEM) image of an uncapped sample. However, the atomic force microscopy (AFM) image of a single QR with \textasciitilde 25 nm radius and \textasciitilde 10 nm height (Fig. 1(b)) shows that the real morphology of a ring structure is volcano-like, where the cylindrical symmetry is broken in the lateral direction and the rim height is anisotropic. On the other hand, ideal ring models are often assumed in order to explain theoretically the finely-spaced energy levels of a QR. For an electron rotating along a one-dimensional widthless orbit, the electron energy for the quantum number of ring orbital angular momentum \((L_e = 0, \pm 1, \pm 2, \ldots)\) is given by,

\[ E^{L_e} = \frac{(\hbar L_e)^2}{2m_e R_e^2}, \quad (1) \]

where \(R_e\) and \(m_e\) are the orbital radius and effective mass of an electron, respectively. When the Coulomb interaction between an electron and a hole is ignored, the exciton energy of a one-dimensional ring can be given by simply adding the hole energy term to equation (1) as
where \( R_e \) and \( m_h \) are the orbital radius and effective mass of a hole in a QR, respectively. Because the effective mass and deformation potential of an electrons and holes differ, it is likely that \( R_e = R_h \), whereby the magnetic flux difference between an electron and a hole can give rise to an excitonic AB effect. In this case, the finely-spaced exciton states become optically active only when \( L_e + L_h = 0 \) (solid lines for the energy levels shown in Fig. 1(c–i)), otherwise all cases of \( L_e + L_h \approx 0 \) are dark states (dotted lines).

When Coulomb interactions are considered, the total energy of an exciton in a QR is dominated by the center-of-mass term, giving an energy for the Coulomb-bound electron-hole pair in a QR as

\[
E_{L, L'} = \frac{(\hbar L_e)^2}{2m_e R_e} + \frac{(\hbar L_h)^2}{2m_h R_h},
\]

where \( M_e = m_e + m_h \), \( L_e = L_e + L_h \), and \( R_e = (m_e R_e + m_h R_h)/(m_e + m_h) \) are the total mass, ring orbital angular momentum, and orbital radius for the center-of-mass exciton, respectively. When the center-of-mass exciton rotates in a QR, all the finely-spaced levels are dark states except for the ground state \( L_e = 0 \). Provided that the level spacing is fine enough to define a density of the states for the energy, equation (3) is analogous to that of a one-dimensional confinement system, i.e., \( D(\varepsilon) = \varepsilon^{-0.5} \) as the level spacing increases. However, as the ring width becomes significant compared to the orbit size, the increase of the level spacing is suppressed gradually. For example, when the radial confinement potential for a finite rim is quadratic \( V(r) \sim (r - R)^2 \), the finely-spaced levels are equally spaced. Therefore, density of the states becomes constant with energy, \( D(\varepsilon) \sim \varepsilon^0 \), as is the case for two-dimensional confinement.

The real confinement potential determined by QR morphology differs, however, from the quadratic form \( V(r) \sim (r - R)^2 \). Recently, cross-sectional scanning tunneling microscopy (X-STM) has revealed that the QR structure is anisotropic and singly-connected\(^{11,12}\). Based on the comprehensive structural analysis, the real QR morphology was modelled with a singly-connected volcano structure, i.e., a dip is present in the center area rather than opening and the height is anisotropic\(^{13–15}\). It is noticeable that the Aharonov-Bohm effect has been observed in spite of the anisotropic height and singly-connected QR structure\(^{17,20}\). Because the electron wavefunction decays rapidly toward the center in the singly-connected volcano-like QR, it becomes effectively identical to the wavefunction in a doubly-connected structure. Furthermore, as the rim height anisotropy breaks the cylindrical symmetry, the radial wavefunction can not be separated from the azimuthal one. In this case, the finely-spaced levels of a volcano-like anisotropic lateral confinement potential \( V(r, \theta) \) are not the eigenstates of \( L_e \) as shown in Fig. 1(c–ii). Consequently, it is plausible to conjecture that the power factor for a real QR follows a quasi-one dimensional density of states, i.e., \(-0.5 < \beta < 0\).

Although the lateral size inhomogeneity of ensemble QDs (Fig. 1(a)) is not significant, the spectral inhomogeneity of ensemble QRs is quite broad due to the anisotropic volcano-like morphology, where the energy ranges from the bandgap of bulk GaAs up to that of AlGaAs. In this case, it was known that the wavefunction is likely to be localized in a crescent-like shape, but the degree of localization depends on the QR morphology\(^{17,20}\). The emission near the barrier originates from a strongly localized state in the QR. However, the crescent-like wavefunction can also extend over the whole rim of a QR with the assistance of tunneling, when the degree of localization becomes moderate. Therefore, it is important that a micro-PL spectrum is selected which is characteristic of an extended wavefunction over the whole rim. In order to evaluate the micro-PL spectrum of a single QR near \( \sim 1.695 \) eV, the potential energy of the electron and the hole were calculated using the volcano-like QR model (Supplementary). Provided that lateral dimensions of a QR are relatively large compared to the vertical, an anisotropic confinement potential \( V(r, \theta) \) can be obtained by using the adiabatic approximation. This adiabatic potential for electrons and holes \( V_{e,h}^{\text{LS}}(r, \theta) \) can be determined for the excited vertical quantum state \( (k = 2) \) (Fig. 2(a) and (b)). Anisotropy makes the confinement levels for \( \theta = 0^\circ \) and 90° different, as shown by white solid lines in Fig. 2(a) and (b). Although a subtle difference is present between the model and a real QR, the micro-PL spectrum of the ground exciton state (\( X_{\infty}^0 \)) near \( \sim 1.695 \) eV can be predicted, i.e., an energy difference between the PL spectrum and the bulk GaAs band gap \( \sim 176 \) meV results from the total confinement energy \( \sim 184 \) meV and the Coulomb interaction \( \sim 8 \) meV\(^{29}\). Consequently, the PL spectrum near \( \sim 1.695 \) eV (Fig. 3) can be attributed to an extended wavefunction over the whole rim although its distribution is anisotropic. The subtle difference can be revised by regarding the Coulomb interaction in the presence of the anisotropy\(^{31}\).

When excitation is strong, we found that an additional high-energy PL peak becomes significant at \( \sim 100 \) meV above the main low-energy PL peak (Fig. 3(a)). We have confirmed that the high-energy PL peak is an excited exciton state \( (X_{\infty}^2) \) by using excitation intensity dependent and time-resolved PL (Supplementary). \( X_{\infty}^2 \) becomes also suppressed as the temperature increases. We have already shown\(^{37}\) that the \( p \) orbital asymmetry of \( X_{\infty}^2 \) gives rise to a large polarization asymmetry and a broad linewidth as a consequence of the strong coupling with phonon bath compared to \( X_{\infty}^1 \). Intermediate spectra between \( X_{\infty}^1 \) and \( X_{\infty}^2 \), where the finely-spaced levels of a ring structure with sub-meV spacing might be seen, are extremely weak. The intra-relaxation in these levels is therefore predicted to be very fast \( \sim 10^8 \) ps\(^{-1}\). This implies that the fractional radiative recombination rate with respect to thermal excitation \( \tau(T) \) within the ground state PL spectrum of \( X_{\infty}^1 \) can be used to estimate the density of the states. For an optical transition between the confined ground states of an electron and a hole in a one-dimensional (1D) or two-dimensional (2D) system, the transition strength of the exciton at \( K = 0 \) (\( F_e \)) can be determined by the oscillator strength \( f_e \) and the wavefunction of the electron with respect to the hole \( \phi(r - r_h) \) as \( F_e \sim f_e |\phi(0)|^2 \). However, as the excitons are scattered by acoustic phonons, a finite linewidth \( \Delta \) is produced. This means that the
transitions are shared within this spectral width $\Delta$. Therefore, the density of states needs to take into account the density of shared transitions ($D(\varepsilon)\Delta$). As the interaction between excitons and acoustic-phonons becomes enhanced by increasing temperature, the linewidth $\Delta(T)$ also depends on temperature. As a result, the stochastic fraction of excitons contributing to recombination within a spectral width $\Delta(T)$ at $T$ can be estimated as

$$r(T) = \frac{\int_{0}^{\Delta(T)} D(\varepsilon)e^{-\varepsilon/k_{B}T}d\varepsilon}{\int_{0}^{\infty} D(\varepsilon)e^{-\varepsilon/k_{B}T}d\varepsilon},$$

(4)

whereby the effective transition strength is given by $\phi_{\text{eff}} \sim f_0 |\phi(0)|^2 \tau(T)/(D(\varepsilon)\Delta(T))^2$. As $\tau(T) \sim (\varepsilon^{2}/\phi_{\text{eff}})^{-1}$, the essential temperature dependence is determined by $\tau(T) \sim \Delta(T)/\tau(T)$. As shown in Figs 3(b) and 4(a), a linear increase in the linewidth was observed up to $\sim 25 \text{ K}$ due to the exciton-acoustic phonon interaction, leading to a monotonic decrease in the time-integrated PL intensity. For $T \gtrsim 30 \text{ K}$, the linewidth broadens exponentially as exciton-optical phonon scattering dominates. Also, the PL intensity decreases significantly as other quenching processes are enhanced with increasing temperature. Therefore, the validity of our analysis is limited to temperatures below $\sim 25 \text{ K}$.

As the time-resolved PL intensity in Fig. 4(b) also decays monotonically for $T \lesssim 25 \text{ K}$, the exciton population ($N$) after transient excitation ($g$) can be described by $dN/dt = -N/\tau$, where the PL decay rate ($\tau^{-1} = \tau_{\text{rad}}^{-1} + \tau_{\text{nr}}^{-1}$) is a sum of the radiative and non-radiative decay rate. With the population in a steady state $N = g\tau$, the time-integrated PL intensity at $T$ is given by $I(T) = N(T)/\tau(T) = g\eta(T)$, where $\eta(T) = \tau/\tau_{\text{rad}}$ corresponds to the quantum efficiency at $T^{25}$. Although $\eta(T)$ is unknown, the ratio of $I(T)$ to $I(5 \text{ K})$ can be used to provide a relative quantum efficiency $\zeta(T)$, i.e., $I(T)/I(5 \text{ K}) = \eta(T)/\eta(5 \text{ K}) = \zeta(T)$. Consequently, the temperature dependence of the radiative decay time can be obtained through the observables $\tau(T)$, $\zeta(T)$, and $\Delta(T)$ as $^{26}$

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**Figure 2.** Adiabatic potential energy of a volcano-like QR for an electron (a) and a hole (b).

**Figure 3.** (a) Temperature dependence of the PL spectrum for the ground ($X^{n=1}$) and first excited ($X^{n=2}$) exciton states in a single QR with strong excitation (2.0 kW cm$^{-2}$). (b) Temperature dependent PL spectrum for the ground exciton states ($X^{n=1}$) with weak excitation (0.6 kW cm$^{-2}$) resulting in no $X^{n=2}$ PL.
**Methods**

GaAs rings were grown on an n-doped GaAs (001) substrate using a molecular beam epitaxy system with an ion getter pump. After thermal cleaning of the substrate under arsenic ambient at 600 °C, a 100 nm-thick GaAs buffer layer and a 50 nm-thick Al<sub>0.3</sub>Ga<sub>0.7</sub>As layer were grown successively at 600 °C. The substrate temperature was decreased to 310 °C, and Ga metal equivalent to 2 monolayer-thick GaAs was introduced to the substrate at the main chamber pressure of ~3 × 10<sup>−10</sup> Torr. When the substrate temperature reached 200 °C, arsenic tetramers were introduced to form GaAs rings. Finally, the rings were capped with 60 nm-thick Al<sub>0.3</sub>Ga<sub>0.7</sub>As and 3 nm-thick GaAs for optical measurements<sup>17,18</sup>. During ring formation, the flux of Ga is equivalent to a GaAs growth rate of 0.5 monolayer/s, and the flux of arsenic is 1.2 × 10<sup>−5</sup> Torr. The PL of a single QR was collected at 4 K using a confocal arrangement, where frequency-doubled (400 nm) Ti:sapphire laser pulses (120 fs pulse duration at an 80-MHz repetition rate) were focused on the QR sample (~6 QRs/m<sup>2</sup>) with a spot-size of 0.8 μm<sup>2</sup>. A time-correlated single photon counting system (TCSPC) was used to obtain the time-resolved PL.
References
1. Mano, T., Kuroda, T., Kuroda, K. & Sakoda, K. Self-assembly of quantum dots and rings by droplet epitaxy and their optical properties. J. Nanophotonics 3, 031605 (2009).
2. Alen, B., Martínez-Pastor, J., Granados, D. & Garcia, J. M. Continuum and discrete excitation spectrum of single quantum rings. Phys. Rev. B 72, 155331 (2005).
3. Warburton, R. J. et al. Giant permanent dipole moments of excitons in semiconductor nanostructures. Phys. Rev. B 65, 113303 (2002).
4. Kuroda, T. et al. Optical transitions in quantum ring complexes. Phys. Rev. B 72, 205301 (2005).
5. Koguchi, N., Takahashi, S. & Chikyow, T. New MBE growth method for InSb quantum well boxes. J. Cryst. Growth 111, 688 (1991).
6. Govorov, A. O., Ulloa, S. E., Karrai, K. & Warburton, R. J. Polarized excitons in nanorings and the optical Aharonov–Bohm effect. Phys. Rev. B 66, 081309(R) (2002).
7. Teodoro, M. D. et al. Aharonov–Bohm Interference in Neutral Excitons: Effects of Built-In Electric Fields. Phys. Rev. Lett. 104, 086401 (2002).
8. Ribeiro, E., Govorov, A. O., Carvalho, W. J. & Medeiros-Ribeiro, G. Aharonov–Bohm Signature for Neutral Polarized Excitons in Type-II Quantum Dot Ensembles. Phys. Rev. Lett. 92, 126402 (2004).
9. Bary-Soroker, H., Enit-Wohlman O. & Imry, Y. Effect of Pair Breaking on Mesoscopic Persistent Currents Well above the Superconducting Transition Temperature. Phys. Rev. Lett. 101, 057001 (2008).
10. Haß, D. et al. Magneto-optical properties of ring-shaped self-assembled InGaAs quantum dots. Physica E 13, 165 (2002).
11. Offermans, P. et al. Atomic-scale structure of self-assembled InGaAs quantum rings in GaAs. Appl. Phys. Lett. 87, 131902 (2005).
12. Offermans, P. et al. Polarized nanostructures formed from self-assembled InGaAs quantum rings. Physica E 32, 41 (2006).
13. Fomin, V. M. et al. Theory of electron energy spectrum and Aharonov–Bohm effect in self-assembled InxGa1−xAs quantum rings in GaAs. Phys. Rev. B 76, 235320 (2007).
14. Kleemans, N. A. I. M. et al. Oscillatory Persistent Currents in Self-Assembled Quantum Rings. Phys. Rev. Lett. 99, 146808 (2007).
15. Fomin, V. M. et al. Electron and exciton energy spectra in self-assembled InGaAs/GaAs ring-like nanostructures. Phys. stat. sol. (b) 245, 2657 (2008).
16. Lin, T.-C. et al. Impacts of structural asymmetry on the magnetic response of excitons and biexcitons in single self-assembled In(Ga)As quantum rings. Phys. Rev. B 80, 081304(R) (2009).
17. Kim, H. D. et al. Asymmetry of localised states in a single quantum ring: Polarization dependence of excitons and biexcitons. Appl. Phys. Lett. 102, 033112 (2013).
18. Kim, H. D. et al. Excited exciton and biexciton localised states in a single quantum ring. Appl. Phys. Lett. 103, 173106 (2013).
19. Lin, C. H. et al. Temperature dependence of time-resolved photoluminescence spectroscopy in InAs/GaAs quantum ring. Appl. Phys. Lett. 94, 183101 (2009).
20. Kim, H. D. et al. Observation of a bi-exciton Wigner molecule by fractional optical Aharonov–Bohm oscillations in a single quantum ring. Nano Lett. 16, 27–33 (2016).
21. Akiyama, H. et al. Thermalization Effect on Radiative Decay of Excitons in Quantum Wires. Phys. Rev. Lett. 72, 924–927 (1994).
22. Hooft, G. W. T. et al. Giant oscillator strength of free excitons in GaAs. Phys. Rev. B 35, 8281–8284, whereby we found the experimental radiative decay time of a bulk can be approximated numerically as $\tau_r(T) \approx T^{3/5}$ (1987).
23. Lee, W. et al. Temperature dependence of the radiative recombination time in ZnO nanorods under an external magnetic field of 6T. Opt. Express 22, 17959–17967 (2014).
24. Feldmann, J. et al. Linewidth Dependence of Radiative Exciton Lifetimes in Quantum Wells. Phys. Rev. Lett. 59, 2337–2340 (1987).
25. Miller, R. C. et al. Luminescence studies of optically pumped quantum wells in GaAs–AlxGa1−xAs multilayer structures. Phys. Rev. B 22, 863–871 (1980).
26. Takamizu, D. et al. Direct correlation between the internal quantum efficiency and photoluminescence lifetime in undoped ZnO epilayers grown on Zn-polar ZnO substrates by plasma-assisted molecular beam epitaxy. J. Appl. Phys. 103, 063502 (2008).

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