Improved search for invisible modes of nucleon decay in water with the SNO+ detector

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This paper reports results from a search for single and multi-nucleon disappearance from the $^{16}$O nucleus in water within the SNO+ detector using all of the available data. These so-called “invisible”
decays do not directly deposit energy within the detector but are instead detected through their subsequent nuclear de-excitation and gamma-ray emission. New limits are given for the partial lifetimes: $\tau(n \rightarrow inv) > 9.0 \times 10^{29}$ years, $\tau(p \rightarrow inv) > 9.6 \times 10^{29}$ years, $\tau(nn \rightarrow inv) > 1.5 \times 10^{28}$ years, $\tau(np \rightarrow inv) > 6.0 \times 10^{28}$ years, and $\tau(pp \rightarrow inv) > 1.1 \times 10^{29}$ years at 90% Bayesian credibility level (with a prior uniform in rate). All but the $(nn \rightarrow inv)$ results improve on existing limits by a factor of about 3.

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I. INTRODUCTION

Baryon number and lepton number are accidental symmetries of the Standard Model, yet to date no process violating baryon number and/or lepton number conservation has been observed. Any proven violation of the baryon number conservation principle would be an important step towards explaining the apparent matter-antimatter asymmetry of the Universe. The decay of nucleons would provide a direct observation of baryon number conservation violation and has been the goal of many experiments for the past several decades [1–3]. The particulars of the possible decay modes and their various branching ratios depend heavily on the chosen model, so we seek to make a model-independent measurement of the partial lifetime through individual decay modes. So-called “invisible” decay modes are those where the decay daughter particles cannot be directly observed, but the nuclei are left in an excited state whose de-excitation does deposit energy into the detector. In water, this signal manifests from the energy deposited by gamma-rays in the 5–10 MeV energy window, to which the SNO$^+$ manifests from the energy deposited by gamma-rays in water, this signal is enhanced by the fact that the detector can be found in [7, 8].

II. THE SNO$^+$ DETECTOR

The SNO$^+$ detector is located underground in Sudbury, Ontario, at a depth of 2070 meters. The detector, which is currently filled with liquid scintillator, had about 1kT target volume of ultrapure water in its first phase of data-taking. This target volume was contained in a 6-meter radius spherical acrylic vessel (AV), which was surrounded by an additional buffer volume of ultrapure water and 9394 8-inch photomultiplier tubes (PMTs) mounted on a steel support structure 9-meters from the center of the AV. The AV is held in suspension through a network of Tensylon ropes anchored both to the laboratory deck above the AV and to the cavity floor. A 7-meter long, 1.6 meter diameter acrylic tube attached at the top of the AV extends the active volume up to the laboratory deck, where the water comes into contact with the gas above it.

The first set of published data from the SNO$^+$ water phase spanned various periods of detector and water system commissioning between May 2017 and December 2017, and as a result included variable levels of radon-induced background [6]. The data presented here includes a subset of the previous data, as well as an additional set of low background data that was taken after the installation of an AV cover gas system, between October 2018 and July 2019. Radon and its daughters can be drawn into the target volume both through diffusion and convection from the liquid/gas interface at the top of the detector. The AV cover gas is a sealed system that uses nitrogen gas to protect the volume above the water in the detector against radon, reducing the radon ingress by at least an order of magnitude. Further details on the detector can be found in [7, 8].

III. DATA SELECTION

The water phase of the experiment represents a transitional period in which the detector was commissioned and prepared to be filled with liquid scintillator. During this phase, the background levels fluctuated due to changes in the water processing and recirculation system, and the data was divided into periods of relatively stable background levels. The ingress of radon into the detector produces an inhomogeneous field of background activity within the detector.

In this analysis, the fiducial volumes in the different periods were re-optimized to further suppress this variable background. Since almost all of the transient radon appeared near the top of the detector, this was done by comparing the distribution of events in an energy side-band sensitive to radon (4–5 MeV) between the upper and lower hemispheres to estimate the population of events related to transient radon distributions in different fiducial volumes. The fiducial volume was then optimized by balancing the statistical uncertainty and the systematic uncertainty related to the residual transient radon events in the fiducial volume. The previously published data consisted of six distinct sets of data, each with their own selected fiducial volumes. In all cases, the new fiducial volume is smaller than the previous one, and one of the data sets was removed entirely for this analysis [6]. A breakdown of the individual data set livetimes and their fiducial volumes is given in Table I. The total livetime across all time periods is $274.7 \pm 1.0$ days.
### TABLE I: Optimized fiducial volume and livetime for each of the included datasets.

| Observable | Period 1 | Period 2 | Period 3 | Period 4 | Period 5 | Period 6 |
|------------|----------|----------|----------|----------|----------|----------|
| R (m) max  | 5.1      | 5.1      | 5.1      | 5.1      | 5.4      | 5.2      |
| Z (m) [min, max] | [-6.0, 1.5] | [-6.0, 1.5] | [-6.0, 1.5] | [-3.1, 1.9] | [-6.0, 2.0] | [-6.0, 3.0] |
| Livetime (days) | 5.0     | 14.6     | 30.2     | 28.9     | 11.2     | 184.8    |

## IV. EVENT RECONSTRUCTION

Detailed optical calibrations of the detector were carried out, and an updated optical model including a new tabulation of the optical attenuation lengths of the AV and water volumes, was developed and applied to the new data set \[^8\]. Additionally, the collective angular response of the PMTs and light concentrators was updated following improved calibrations. This new modelling was only applied to the newly acquired period 6 data and associated simulations, resulting in different reconstruction systematic uncertainties for the old and new data.

Event reconstruction does not differ greatly from the previous results, and involves reconstructing the most likely position ($\vec{R}$), direction ($\vec{U}$, orientation of the momentum vector), and effective electron-equivalent kinetic energy ($T_e$) of an event in the detector based on the arrival time of photons at the PMTs, assuming those photons to be electron generated Cherenkov light. Two additional quantities, the in-time-ratio (ITR) and the light isotropy $\beta_{14}$, were used to help identify poor fits and non-physical events (such as those caused by the detector electronics). These two are as previously described in \[^6\] and the same selection criteria of $\text{ITR} > 0.55$ and $-0.12 < \beta_{14} < 0.95$ in \[^6\] are retained for this analysis. Additionally, several new reconstruction figures of merit were used to identify poorly reconstructed event positions and energies.

Systematic uncertainties arising from the detector modelling and event reconstruction were evaluated using $^{16}\text{N}$ calibration data. Changes in the optical calibration between the previous data set (periods 1 through 5) and the newest data set (period 6) require evaluation of that calibration data using the two different models. The improved optical modelling used in the newer data set improved the energy scale and resolution uncertainty by a factor of 2. Additionally, the uncertainty in the calibration source position was applied as an offset in the newer data set as opposed to folding it in with the overall position scale uncertainty.

A summary of all of the systematic uncertainties, split by data-taking period, is given in Table II.

## V. BACKGROUND MODEL

For each of the hypothetical decay modes considered here, the primary detector signature would be one or more gammas depositing a characteristic quantity of energy. In order to identify such events, it is necessary to understand (and thereby account for) various sources of background within the chosen energy window (5–10 MeV).

### A. Instrumental background

Low-level data checks were performed to identify and remove spurious events due to instrumentation and other non-physics sources. These data-cleaning cuts entail a small signal sacrifice and an associated contamination that must be taken into account. The signal sacrifice was determined using the $^{16}\text{N}$ calibration source for each data set, and varies due to the different fiducial volumes. Residual contamination was estimating using a data-driven analysis which compared two sets of data-cleaning cuts using a bifurcated analysis technique. In this technique, the data was separated into 4 categories based on whether it passed or failed two branches of data-cleaning. One branch consisted of a set of low-level data-cleaning cuts based on the hit-times and charge recorded for an event, while the other used the reconstruction classifiers ($\beta_{14}$ and ITR). Based on the individual leakage of these two branches the resulting sacrifice and contami-
TABLE II: Summary of the evaluated systematic uncertainties for the reconstructed parameters, for the various data sets. Due to updates in the optical modeling, the final data set (6) has a separate evaluation of these uncertainties from the previous data sets (1 - 5).

| Parameter          | Uncertainty (1 - 5) | Uncertainty (6) |
|--------------------|---------------------|-----------------|
| x offset (mm)      | +16.4 - 18.2        | +50.1 - 55.6    |
| y offset (mm)      | +22.3 - 19.2        | +47.7 - 59.6    |
| z offset (mm)      | +38.4 - 16.7        | +75.8 - 34.7    |
| x scale (%)        | +0.91 - 1.01        | (x > 0) +0.16  |
|                    |                     | (x < 0) +0.17  |
| y scale (%)        | +0.92 - 1.02        | (y > 0) +0.12  |
|                    |                     | (y < 0) +0.22  |
| z scale (%)        | +0.91 - 0.99        | (z > 0) +0.30  |
|                    |                     | (z < 0) +0.42  |
| x resolution (mm)  | 104                 | $\sqrt{3214 + |0.393x - 290|}$ |
| y resolution (mm)  | 98                  | $\sqrt{2004 + |0.809y - 1365|}$ |
| z resolution (mm)  | 106                 | $\sqrt{7230 + |0.730z + 3211|}$ |
| Angular resolution | +0.13               | +0.122          |
| $\beta_{14}$       | +0.005             | +0.005          |
| Energy scale (%)   | 2.0                 | 1.02            |
| Energy resolution  | +0.018             | +0.0084         |
|                    | -0.016             | -0.0079         |

TABLE III: Fraction of signal sacrificed by data-cleaning cuts and the corresponding number of non-physical events expected to pass the signal selection criteria, as evaluated from the physics data and calibration data.

| Dataset | Sacrifice       | Contamination (events) |
|---------|-----------------|------------------------|
| 1       | (1.2 ± 0.3)%    | 0.01 ± 0.02            |
| 2       | (1.2 ± 0.3)%    | 0.04 ± 0.03            |
| 3       | (1.2 ± 0.3)%    | 0.03 ± 0.03            |
| 4       | (1.2 ± 0.3)%    | 0.08 ± 0.06            |
| 5       | (1.3 ± 0.3)%    | 0.01 ± 0.01            |
| 6       | (1.7 ± 0.4)%    | 0.04 ± 0.01            |

The estimated contamination and sacrifice with the updated reconstruction and systematics are consistent with previous estimates using this technique.

B. Cosmogenic background

The depth of the SNO+ detector reduces the total muon flux in the detector to only about 3 muons per hour. This is a vital advantage in the search for invisible nucleon decay, since muon spallation reactions producing $^{16}$N yield an event signature that is almost identical to the nucleon decay signal. Therefore, it is important to remove the remaining cosmogenic $^{16}$N events by muon identification and a 20-second cut on events after each detected muon. Based on an estimated cosmogenic rate from [9, 10], scaled to the SNO+ detector depth, and the 20-second muon veto cut, there is 1 event expected within the fiducial volume, across the cumulative livetime of the data sets.

C. Radioactive background

The dominant background in this analysis is due to trace levels of residual contamination from uranium and thorium, as well as radon ingress, that primarily manifest as $^{214}$Bi and $^{208}$Tl decays. The majority of these events fall below the 5–MeV analysis threshold.

The radioactivity intrinsic to the internal water was fit as two individual components, $^{214}$Bi and $^{208}$Tl. The presence of the AV cover-gas system reduced the internal $^{214}$Bi (U-chain) and $^{208}$Tl (Th-chain) levels by one order of magnitude compared to the previous analysis [6], with current values of $(5.78\pm0.7^{+1.5}_{-1.3})\times10^{-15}$ gU/g and $<4.8\times10^{-16}$ gTl/g (95% C.L.), respectively.

For this analysis, all of the decays external to the target volume were treated as a single parameter in the fit. This single parameter includes contributions from decays in the external water, the AV, and the ropes that hold the AV in place. Glass in the PMTs has higher radioactivity relative to other detector components, but the approximately two and a half meters of external water between the PMTs and the fiducial volume attenuates this contribution to detector background to a negligible level, and so this background was not included in the fit.
D. Neutrino background

Several sources of neutrino and antineutrino background were present, which were constrained through previous experimental results and data. The most significant source of background comes from $^8$B solar neutrinos, which have been well measured. For these results, the solar neutrino flux is constrained based on recent results from Super-Kamiokande [11], which are consistent with both the SNO [12] and SNO+ [13] measurements, with oscillations applied using the BS2005-OP solar model [14].

Atmospheric neutrino interactions also create signals within the detector through neutral current interactions that can liberate nucleons from the oxygen nucleus. The subsequent de-excitation of $^{15}$N* or $^{15}$O* could look identical to the single proton and neutron decay modes. However, many of these interactions can be identified by detecting the neutron captures that follow the event. Estimates based on GENIE simulations [15] predict about 0.1 interactions produce an excited state nucleus per day within the entire internal water volume. By comparing the uncertainty on the atmospheric neutrino flux, GENIE branching ratio, and the interaction cross-section, a 67% total uncertainty on the normalization of the atmospheric contamination rate was found.

Antineutrinos from the nearby nuclear reactors were also considered in the analysis, though their overall contribution was relatively small. The flux estimates combined reactor information from the International Atomic Energy Agency [16] with Canadian reactor power information [17] to provide a constraint. Furthermore, because the reactor signals are inverse beta decays, the neutron follower cut designed to reduce the number of atmospheric events served to also reduce the reactor antineutrino background. The total number of reactor antineutrino background events was fit in the analysis with the included constraint from the flux, yielding an estimate of 1.8 events summed across all of the data sets within the fiducial volumes.

E. Additional subdominant backgrounds

Other backgrounds were studied and found to be negligible in magnitude and not included in the fit. These backgrounds would not normally fall within the region of interest, but can occasionally do so due to misreconstruction. From Monte Carlo simulations, the PMT background is expected to contribute fewer than 0.1 events within the region of interest in the entire data set. The other considered sources of subdominant background were ($\alpha$,n) reactions on $^{13}$C (acrylic) or $^{18}$O (acrylic and water) nuclei. In the $^{13}$C case, an $\alpha$ is captured on the nucleus, resulting in a neutron and a $^{16}$O nucleus, which can be produced in an excited state of 6.1 MeV up to 10% of the time. The gammas or electrons/positrons emitted in the de-excitation have a small chance of falling into the region of interest (ROI) for this study. However, the reaction on $^{18}$O produces low energy gammas and, therefore, it is expected to make a negligible contribution in the ROI. The dominant source of alphas is from $^{210}$Po embedded a few nanometers below the AV surface [7].

In total, there are expected to be fewer than 1.4 events out of a total of 239 in the data set that are not included in the fit. The expected contribution from these backgrounds are not subtracted from the final signal count, producing a more conservative upper limit on the nucleon decay lifetimes.

VI. ANALYSIS METHODS

This analysis applied new selection criteria to the previous data (consisting of data sets 1 through 5), with the addition of the sixth blinded data set. Data was blinded in the approximate energy range of 5 to 15 MeV based on the number of PMT hits per event. The region outside of the blinded region (unblinded data) was used for a fiducial volume selection study. As a result of radon ingress from the gas/liquid interface above, the spatial field of background radioactivity in the detector was not homogeneous, and so it was necessary to limit the fiducial volume by placing a varying cut in Z for each of the data sets independently. Since these asymmetries are not modeled in Monte Carlo simulations, an analysis on data outside of the region of interest, from 4–5 MeV, was used to assess this top-bottom asymmetry and select a fiducial volume that would minimize the uncertainty due to this event contamination. The event selection criteria for each of the individual data sets is given in Table I.

Events within the selected ROI between 5 and 10 MeV were fitted using an unbinned maximum likelihood method with probability distributions produced from the Monte Carlo in energy, position, and direction. The normalization on the signal rate and the rate of internal and external radioactive backgrounds were fit unconstrained, while the cosmogenic $^{16}$N, atmospheric neutrino, and solar neutrino events included a Gaussian constraint as discussed in the previous section. The fitting technique was repeated for each of the signals of interest ($n$, $p$, $pp$, $pn$, and $nn$ decay) independently. The Monte Carlo model simulates events uniformly in time throughout the data taking window, including variations in the detector state. The probability distribution functions (PDFs) were separated into a one-dimensional distribution in $R^3$ multiplied by a two-dimensional distribution in ($\cos \theta_{\text{sun}}$, $T_e$), where $\cos \theta_{\text{sun}}$ is the dot product between the reconstructed event direction and the position of the sun with respect to the event position. The choice to split the full PDF this way was due to the strong correlation between $\cos \theta_{\text{sun}}$ and $T_e$ found in the solar neutrino background (due to the decreasing opening angle between the electron and the incident neutrino in the elastic scattering process), and the relatively weak correlation with respect to position.
FIG. 2: Projection of the reconstructed energy (left) and the dot product of the reconstructed direction and the solar direction (right) for the entire data set. The error bands on the total fit show the result of all of the systematic uncertainties applied. The neutron decay signal shown is at the best-fit lifetime of $1.7 \times 10^{30}$ years.

To evaluate the effect of the systematic uncertainties on the reconstructed parameters, the probability distributions for each signal and background were reconstructed with each parameter varied by one standard deviation in each direction as given in Table IV. The full data was then refitted with each of the new sets of PDFs, and the difference between the new best-fit signal and the nominal best-fit taken as the systematic uncertainty on the number of signal counts. The nominal likelihood function was then convolved with an asymmetric normal distribution, whose width was determined by the quadrature sum of these systematic uncertainties. The signal upper limit is then determined by directly integrating the likelihood function, with a positive uniform prior in rate, up to the 90% interval.

VII. RESULTS

Results for the upper limit on the 5 decay modes of interest, including systematic uncertainties, are evaluated independently and given in Table IV. The total $T_e$ and $\cos \theta_{\text{sun}}$ spectra for the combined data set for the neutron decay mode are shown in Figure 2, where the bands on the total spectrum show the effect that the systematic uncertainties have on the final spectral shape. The signal likelihood is shown in Figure 1 which in each of the studied decay modes is consistent with no observed signal.

VIII. CONCLUSION

Multiple data sets totalling 274.7 days of data-taking were analyzed to search for five selected modes of “invisible” nucleon decay ($n$, $p$, $nn$, $pp$, $pn$). Results are consistent with no observation of invisible nucleon decay for all the studied decay modes, and represent an improvement on previous limits for all but the $nn$ decay mode. In particular, the addition of the longer low-background data set improved the previous SNO+ results on the $n$ and $p$ decay modes by a factor of 3 while improving the $pn$ and $pp$ decay modes by a factor of 2 [6].

| Decay Mode | Partial Lifetime Limit | Existing Limits |
|------------|------------------------|-----------------|
| $n$        | $9.0 \times 10^{29}$ y  | $5.8 \times 10^{29}$ y [5] |
| $p$        | $9.6 \times 10^{29}$ y  | $3.6 \times 10^{29}$ y [6] |
| $pp$       | $1.1 \times 10^{29}$ y  | $4.7 \times 10^{28}$ y [6] |
| $np$       | $6.0 \times 10^{28}$ y  | $2.6 \times 10^{28}$ y [6] |
| $nn$       | $1.5 \times 10^{28}$ y  | $1.4 \times 10^{30}$ y [5] |

TABLE IV: Lifetime limits at 90% C.I. for the invisible decay modes of interest alongside the existing limits.

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