Quantum systems as used for quantum computation or quantum sensing are nowadays often realized in solid state devices as e.g. complex Josephson circuits or coupled quantum-dot systems. Condensed matter as an environment influences heavily the quantum coherence of such systems. Here, we investigate electron transport through asymmetrically coupled InAs double quantum dots and observe an extremely strong temperature dependence of the coherent current peaks of single-electron tunneling. We analyze experimentally and theoretically the broadening of such coherent current peaks up to temperatures of 20K and we are able to model it with quantum dissipation being due to two different bosonic baths. These bosonic baths mainly originate from substrate phonons. Application of a magnetic field helps us to identify the different quantum dot states through their temperature dependence.
The building blocks of quantum information technology and future quantum computers are qubits. Qubits can be based on coherent superpositions in double quantum dots (DQD) and such DQDs can be easily formed in a variety of semiconducting materials. The use of semiconductor technology guarantees more or less the necessary scalability of qubit structures. Along these lines, it has been shown recently that qubits based on quantum dots can be formed and manipulated in CMOS technology at not very low temperatures, i.e., quantum-dot-based quantum computers seem to be within reach. The first observation of a coherent mode in a DQD system dates back more than 20 years, while successful coherent manipulation of electronic states or of spin states in DQDs has been shown a few years later, opening the path towards quantum information processing with quantum dots.

Coherence properties of a quantum state depend on the influence of the environment. Already in the early studies of DQDs it became clear that they interact with the environment via the emission of phonons. Measurements of phonon emission were repeated in more detail just recently. Whereas in these works coupling to the phonon bath has been studied in great detail for detuned quantum dots, corresponding studies just at the resonance are scarce. In addition to the mentioning of some temperature dependence of the so-called elastic peak in refs. and a theoretical work studied phonon decoherence in 2005; and it has been shown that at low temperatures, electron-phonon scattering can enhance the current noise close to resonance, as has been discussed experimentally and theoretically.

Here, we focus on the detailed temperature dependence of the resonant tunnel current, which is mainly caused by the coupling to the phonon environment. We describe the quantum dissipation of the coherent current peaks up to temperatures of 20 K by introducing couplings to two different bosonic baths.

Results

Experiment. For our studies, we use self-assembled InAs quantum dots similar to the ones used in refs. and . The second quantum dot grows on top of the first dot due to strain fields induced by the InAs islands. The second dot is slightly larger than the first. AlAs layers of nominally identical thickness are used to separate the InAs quantum dots from the doped GaAs layers and from each other, as depicted in Fig. 1b. However, as visible in the transmission electron microscope image, the quantum dots penetrate into the barriers, therefore reducing the effective barrier thickness, resulting in an asymmetric coupling to the leads. Similar devices show typical quantum-dot (QD) diameters of 10 nm $\lesssim d \lesssim 20$ nm with heights of $2 \text{ nm} \lesssim h \lesssim 4$ nm.

The charging and quantization energies are expected to be of the order of 20 meV. However, the parameters feeding into these configurations for each individual DQD. Each characteristic feature in the current is expected to arise from a single DQD channel, although several dots are present, see e.g., refs. and similarly for single dot devices.

The line plot in Fig. 1a shows the current $I$ through the DQD device as a function of the bias voltage $V$ for different temperatures ranging from 1.5 to 21 K. The graph shows two distinct current peaks at $V \approx 155$ mV (peak I) and $V \approx 187$ mV (peak II), which are due to the resonant tunneling of single electrons through the InAs double quantum dots. The left peak (see also left schematic level diagram in Fig. 1a) corresponds to only a single electron being present in the DQD and originates from tunnel cycles with the occupation $(0,0) \rightarrow (1,0) \rightarrow (0,1)$. This situation is depicted in the charging diagram in Fig. 1e as the triple point I. The right peak in Fig. 1a corresponds to single-electron tunneling through an additional electron being present and including double occupation, namely $(1,0) \rightarrow (2,0) \rightarrow (1,1)$ (see right schematic level diagram in Fig. 1a and triple point II in the charging diagram in Fig. 1e).

Even though in a simplified understanding of single-electron tunneling through DQDs, the tunnel resonances should not be affected by the Fermi distributions in the leads due to the low temperatures and the resonances being far away from the Fermi levels in the leads, we observe a quite strong temperature dependence of both the amplitude and the width of both peaks in Fig. 1a. With increasing temperature, the current resonances significantly broaden and at the same time the amplitude of the peaks decreases. Both effects are accompanied by a shift of the peak position toward slightly more positive voltages. This shift is attributed to temperature-dependent changes in the electric field distribution in the sample.

Whilst both resonances show similar behavior as a function of temperature, the magnetic field dependence reveals major differences. The color graphs in Fig. 1c, d show the current of the respective resonance as a function of bias voltage and magnetic field up to $B = 2$ T at $T = 1.5$ K. For peak I, the main effect of the magnetic field seems to be a reduction of the peak amplitude. The magnetic field was applied perpendicular to the layer structure and parallel to the current. Therefore the weak oscillation observed for the magnetic field dependence of the resonances originates from the Landau-level structure in the emitter. For peak II (Fig. 1d), not only is the amplitude much less affected in comparison to the first peak, but the single resonance splits into two. This indicates that the two peaks emerge from different electron configurations, where the left peak I correspond to a single-electron triple point, whereas the right peak II involves a double occupation of the larger quantum dot. In the charging diagram in Fig. 1e two more triple points appear, which are not expected to be observable in our structure. Triple point IV will be spin blocked, whereas triple point III corresponds to hole-transport, which exchanges the role of the asymmetric couplings, and therefore, these current peaks will be much smaller.

For now, we want to focus on the temperature dependence of the resonances. However, not only the peaks in the current are influenced by increasing temperature, but also the off-resonant background current experiences a temperature-dependent increase. Especially for the right peak II and the highest temperatures, the increasing background current interferes with the appearance and the visibility of the resonance peak. In order to analyze the current resonances in more detail, we subtracted this temperature-dependent background as outlined in Supplementary Note II: Data analysis and will discuss it later. In Fig. 2 the current resonances are presented after subtraction of the background current and after normalizing to the peak position. For three temperatures, peak I is presented in Fig. 2a, whereas in Fig. 2b peak II is shown. For both peaks, one sees a clear decrease in amplitude and an increase in broadening with temperature. This trend has been observed also in a sample of similar layer structure discussed in Supplementary Note I: Additional data.

Theoretical model. For a theoretical description, we model each quantum dot as a single orbital with energy $E_\ell = L, R$ and tunnel coupling $\Omega$. For states with more than one electron, we consider the onsite and nearest-neighbor interaction energies $U$ and $U'$, respectively. Each dot is tunnel coupled also to a lead which allows electron transitions with the rates $\Gamma_\ell$ from lead $\ell = L, R$ to the dot and back, depending on the Fermi energy of the respective lead. For sufficiently small tunnel coupling, the leads are eliminated within a Bloch-Redfield approach, which...
Fig. 1 Experiment. a Current-voltage characteristic of InAs double quantum dots (DQDs) for different temperatures between 1.5 and 21 K. The inset shows simplified energy level diagrams of the DQD system: the left diagram for the first resonance peak (peak I) around 155 mV and the right diagram for the second resonance peak (peak II) around 188 mV. b Transmission electron microscope image of a DQD device of similar layer structure and schematic image of the investigated heterostructure and the measurement setup, see methods section for detailed information. c Current of resonance I as function of voltage and magnetic field at $T = 1.5$ K. d Same for resonance II. e Charging diagram of the double quantum-dot system with all the triple points involving one and two-electron states. The different couplings to the two leads are depicted by arrows with different colors and thicknesses.

Fig. 2 Analysis of the current peaks. a, b Enlargement of the measured peaks at $V_0 = 155$ mV (peak I) and $V_0 = 188$ mV (peak II), respectively, with the background subtracted (solid lines) in comparison with the result of the theoretical prediction with only bath 1 (dashed) for various temperatures. The inset of panel b reveals the presence of two further resonances. c Corresponding model with an environment coupled to the difference of the onsite energies. d, e Width $\Delta$ and height $I_{\text{max}}$ of peak I in dependence of the temperature. Experimental values are depicted by circles while the dashed line shows the current of the full model with $\Gamma_L = 500$ $\mu$eV, $\Gamma_R = 40$ $\mu$eV, $\Omega = 4.2$ $\mu$eV, $a = 0.01$, and $\alpha' = 0$.

leads to a master equation for the reduced density operator of the DQD on a many-body basis. Here, the relatively small inter-dot tunneling in the experiment requires us to work beyond a secular approximation, i.e., to take off-diagonal density matrix elements into account. For a detailed description of the formalism, see Methods Section.

Quantum dissipation is modeled by coupling to bosonic degrees of freedom with the Hamiltonian $H_{\text{el-env}} = \mathcal{Z} \xi$ with the (dimensionless) DQD dipole operator $Z = n_L - n_R$ and $n_L = 1, 2$ the occupation of dot $\xi$, as sketched in Fig. 2c. The quantum noise $\xi = \sum \lambda_\nu (a_\nu^\dagger + a_\nu)$ originates from bosonic modes $\nu$ with frequency $\omega_\nu$, annihilation operator $a_\nu$, and coupling strength $\lambda_\nu$. We assume the modes to be initially at thermal equilibrium with temperature $T$. The corresponding rates for dissipation and decoherence can be expressed in terms of the spectral density $\mathcal{J}(\omega) = n \sum \lambda_\nu^2 \delta(\omega - \omega_\nu) \equiv n \omega_\nu \lambda_\nu / 2$, where we assume to be Ohmic, i.e., linear in the frequency $\omega$. A particular role is played by the dimensionless dissipation strength $\lambda$, which determines the magnitude of dissipation and decoherence. One of our main goals is to determine $\lambda$ from experimental data. Let us remark that the DQD-bath model has been chosen such that for the DQD occupation with a single electron, the tunnel term in $H_{\text{DQD}}$ and the coupling operator $Z$ can be represented by the Pauli matrices $\sigma_x$ and $\sigma_z$, respectively. Then our Hamiltonian becomes the usual Caldeira-Leggett model $H = \frac{1}{2} \sigma_x + \frac{1}{2} \sigma_z + \sigma_z \xi$ for the dissipative two-level system with detuning $\epsilon = \epsilon_L - \epsilon_R$. It undergoes a phase transition at $\alpha = 1$, while for $\alpha \ll 1$, its dynamics is governed by quantum coherence.

For a strong detuning of the DQD levels, the dipole operator $Z$ is practically a good quantum number, i.e., it approximately commutes with the DQD Hamiltonian and, thus, cannot cause significant transitions. Therefore, as we will see in our numerical results, $H_{\text{el-env}}$ may explain the broadening of the peaks, but not the emergence of the temperature-dependent background. To model the latter, we introduce a second heat bath with the Hamiltonian $H_{\text{el-env}}' = X \sum \lambda_\nu (b_\nu^\dagger + b_\nu)$, where the annihilation operator $b_\nu$ is the spectral density, and the dimensionless dissipation strength $\alpha'$ are defined as for the first bath. The coupling is established via the tunnel operator $X = \sum \epsilon_\nu (c_{\nu L}^\dagger c_{\nu R} + c_{\nu R}^\dagger c_{\nu L})$ and,
thus, can induce dissipative transitions of electrons from one QD to the other. Hence, this bath is relevant mainly when the DQD eigenstates are localized, i.e., far from the peaks where the detuning dominates. Physically, this corresponds to coupling the intra-dot current to an environment.

**Peak broadening.** The most significant observation in the measured current peaks is their broadening with increasing temperature. After subtraction of the background, the peaks reveal a Lorentzian shape, see Fig. 2a, b. In panel b, we also witness that with increasing temperature, the Lorentzian may be distorted by small resonances in its vicinity. Our first goal is to determine the tunnel couplings \( \Gamma_{1,R} \) and \( \Omega \) as well as the dimensionless dissipation strength \( \alpha \). Without the background, it turns out to be sufficient to consider only bath 1. The task is facilitated by the approximate solution for the current

\[
I \approx \frac{e}{\hbar} \frac{\Omega^2 \left( y - 2\pi \alpha c \right)}{4c^2 + \left( y + 2\Omega^2 / \Gamma_R \right)^2} \tag{1}
\]

with \( y = \Gamma_R + 4\pi \alpha c \omega \) and the detuning \( \epsilon = \eta (V - V_{\text{peak}}) \) with the peak position \( V_{\text{peak}} \) and the leverage \( \eta = 0.15 \). For a derivation, see Supplementary Note IV: Three-level approximation. Then for the relatively large temperatures in our experiment, the peak as a function of the detuning \( \epsilon \) has the width \( y \), while its height reads \( \Delta I^2 / \hbar y \). Hence, from the linear behavior of the width of peak I as a function of \( T \) (Fig. 2d), we can immediately read off \( \Gamma_R = 40 \mu eV \) and \( \alpha = 0.01 \), which in our sample is clearly larger than in lateral GaAs QDs. With these parameters at hand, the peak height shown in Fig. 2e provides the inter-dot tunneling \( \Omega = 4.2 \mu eV \). Quite remarkably, the tunneling from the emitter, \( \Gamma_L \), is of minor relevance, as long as \( \Gamma_L \gg \Gamma_R \) showing the dominance of the smallest rate in tunneling. Using these values, the theoretical results for the shape of the peaks agree rather well with the experimental data.

For peak II, the determination of the width at high temperatures is hindered by the emergence of two small, but close peaks visible in the inset of Fig. 2b. Nevertheless, we find that the above values for \( \Gamma_i \) and \( \alpha \) predict also the width of this peak. However, matching the peak height requires a significantly smaller inter-dot tunneling \( \Omega = 1.8 \mu eV \). This indicates that the two peaks investigated stem from different DQDs. Moreover, if peak II were due to the two-electron resonance of the same DQD, it would lie on the left-hand side of peak I, as we demonstrate in Supplementary Note III: Charging diagram and current.

**Background.** We have seen that the coupling to a heat bath via the DQD dipole moment can provide a faithful description of the broadening of the resonance peaks. However, it does not explain the smooth, temperature-dependent background witnessed in the experimental data shown in Fig. 1a and detailed in Fig. 3a. We attribute this background to a weak coupling of the inter-dot current to an environment modeled by our second bath. In the following, we estimate the corresponding dissipation strength \( \alpha' \). To compensate for the impact of other double dots in our sample, we focus on how the baseline of the peak raises from its value at the lowest temperature used in the experiment, 1.5 K, which provides the data in Fig. 3d. For the theoretical analysis, we now include also the dissipative inter-dot tunneling sketched in Fig. 3c.

For the fitting, we again start with an analytic estimate. In doing so, we derive with a standard calculation (Supplementary Note V: Analytical expression for the background) the dissipative transition rate between the states (1, 0) and (0, 1), which reads \( \kappa(\epsilon) = \pi \alpha' c / \hbar (1 - e^{-\epsilon / kT}) \). Since these dissipative transitions are rather slow, they represent the bottleneck of the transport and determine the current such that \( I \sim \kappa(\epsilon) \). For the dissipation strength \( \alpha' = 2.2 \cdot 10^{-6} \), the theory result for \( \Delta I \) agrees with our experimental data. Remarkably, already for \( \alpha' \sim 10^{-4} \alpha \), the second bath has a significant influence. This is in agreement with previous theoretical findings that a heat bath that couples via the tunnel operator may have a rather strong impact already for small values of \( \alpha' \). The comparison of the theoretically computed background in Fig. 3b exhibits a qualitative agreement with experimental data. On a quantitative level, however, the shape of the background is reproduced by the model, not as well as the peak itself. One reason for this is that the impact of neighboring DQDs cannot be isolated with sufficient precision. Another reason is that in contrast to bath 1, the present dissipative decay probes the spectral density of the bath in a broad frequency range. Therefore, the assumption of an Ohmic monotonic spectral density naturally implies limited agreement. Nevertheless, our model is capable of explaining the physics that leads to the background of the current peaks.

**Zeeman splitting.** Both current peaks analyzed above may be fitted with either a one-electron model or with a model with up to two electrons. However, as indicated in Fig. 1c, d, both lead to different behavior in the presence of a magnetic field. Specifically, peak II splits up, while peak I does not, at least not at 1.5 K. To analyze the impact of a magnetic field in more detail, we add a Zeeman term to our model and elaborate on the resulting temperature dependence of the peaks.

While in our experiment, the magnetic field is homogeneous, the \( g \)-factors of the dots are different due to the different sizes of the two dots, and such the Zeeman splitting becomes inhomogeneous. With the observed splitting of \( \Delta V \approx 2.2 \text{ mV at } B = 0.4 \text{ T} \), and the leverage factor \( \eta = 0.15 \), we calculate \( \Delta g = 1.42 \), which seems reasonable in comparison to single dot devices of similar size. The details of the individual \( g \)-factors are not observed in our experiment. We use in our model as parameters the average...
Zeeman energy $E_Z$ and their difference $\Delta E_Z$. Provided that the Zeeman splitting does not shift any energy level across the Fermi surface, $E_Z$ has no relevant influence. Hence, an appropriate extension of the model can be described by the Hamiltonian $H_{\text{Zeeman}} = \frac{1}{2} \Delta E_Z (n_{\uparrow \uparrow} - n_{\uparrow \downarrow} - n_{\downarrow \uparrow} + n_{\downarrow \downarrow})$, where $\Delta E_Z$ is determined from the splitting of the peak.

Figure 4 depicts the corresponding measured (panels a and b) and computed (panels c and d) current peaks for various temperatures. As already seen in Fig. 1b, at $T = 1.5 \text{ K}$ we witness a single peak, while Fig. 4a shows that with increasing temperature, a second peak emerges. This observation can be explained with the level scheme sketched on top of the experimental plots. For an inhomogeneous Zeeman splitting, the transport channels cannot be resonant at the same time. Hence, an electron may get stuck in the off-resonant channel and block transport. However, owing to the coupling to the bath, a dissipative decay ($\downarrow, 0$) → ($\downarrow, 1$) can resolve the blockade such that a current can flow. For the spin-up channel, however, the corresponding process requires the absorption of energy from the bath and, therefore, can occur only at sufficiently high temperatures. The results obtained with our theoretical model qualitatively explain the emergence of the second peak in the temperature regime of the experiment. In the numerical data, however, the second peak is poorly resolved, as only a small shoulder emerges. For this discrepancy between theory and experiment, two possible reasons come to mind. First, the magnetic field may distort the electron wave function such that the dissipation strength $\alpha'$ becomes larger and, thus, dissipation-assisted tunneling is enhanced. The dashed line in Fig. 4c shows with larger $\alpha'$ indeed a double peak emerges. A further possible explanation is that with increasing Zeeman splitting, spin flips caused by the strong hyperfine interaction in InAs$^{21}$ may play an important role. Then an electron in the blocked channel can undergo a spin flip and, thus, end up in the resonant channel. The dotted line in panel c demonstrates that also this conjecture leads to a double peak (details of the corresponding model are given in Supplementary Note VI. Additional spin flip noise).

For peak II, this kind of current blockade does not occur, because the resonant state in the left QD is the spin singlet $(\uparrow, \downarrow, 0)$ which is unaffected by the magnetic field. Hence, we observe a double peak also at low temperatures. With increasing temperature, each peak broadens much like the single peaks obtained in the absence of a magnetic field.

Conclusions

We have measured resonance peaks in the current through InAs double quantum dots and showed how their width and background increase with temperature in the range of $1.5-21 \text{ K}$. This behavior can be fully explained by introducing two (bosonic) baths of the Caldeira-Leggett type. The peak broadening can be modeled with rather good precision with a bath that couples via the dipole moment of the DQD. Far from the peak, however, this bath has little influence. Therefore, we introduced a second bath that couples to the DQD current, which in a tight-binding description, is given by the tunnel operator. We determined the corresponding dimensionless dissipation strength of each bath. Physically, the baths describe the influence of substrate phonons and also of the impedance of the electromagnetic environment$^{32,33}$.

A magnetic field makes the situation more complex. In particular, we found that then the behavior of the peaks depends on the triple point at which the DQD is operated. In turn, this allows one to determine whether two-electron states play a role.

The interest in the dissipative model parameters extends beyond the description of current peaks. For example, with the dot-lead couplings suppressed, the one-electron states form a charge qubit whose dephasing time as a function of the dissipation strength is given by the corresponding rates in the quantum master equation (see the Supplementary Note VII: Dephasing time of a charge qubit) and in the absence of the second bath is known analytically$^{27,34}$. In the temperature regime of the experiment, the present values of $\alpha$ and $\alpha'$ correspond to a dephasing time of the order $T_2 \sim 100 \text{ ps}$, where the precise value depends also on the detuning. Assuming that the same model parameters are valid at lower temperatures, one can predict coherence times up to 10 ns. Therefore, our analysis allows us to determine parameters being essential for all approaches involving the manipulation of quantum states.

Methods

Experiment. The experimental device consists of self-assembled InAs double quantum dots, stacked between GaAs leads with annealed metal contacts. Three AlAs layers of nominally identical thickness 5 nm are used to separate the two InAs quantum-dot layers from the (doped) GaAs leads and from each other. Temperature and magnetic field control were achieved by placing the device into a He4 cryostat with a variable temperature insert. For all measurements, the bias voltage was applied to the contact closer to the layer of smaller QDs (right). The other contact, which is closer to the larger QDs (left) was connected to a current preamplifier ($1 \times 10^{-13} \text{A V}^{-1}$) to ensure high sensitivity. Each datapoint was obtained by integrating the voltage output of the current preamplifier over one power line cycle (20 ms).

Bloch-Redfield master equation. The full model Hamiltonian for the DQD and its environment is of the structure $H = H_{\text{DQD}} + H_{\text{env}} + V$, where $H_{\text{DQD}}$ and the DQD-environment coupling $V$ contain a summation of all heat baths and leads. The dynamics of the total density operator is governed by the Liouville-von Neumann equation $\dot{\rho} = -\frac{\hbar}{i} [H, \rho] + \sum_{\alpha} \frac{\hbar}{\tau_{\alpha}} (\rho \otimes \rho_{\alpha} ) - (\rho_{\alpha} \otimes \rho)$. Therefore, we derive a master equation for the density operator of the DQD by integrating out the environment within second-order perturbation theory, which in units with $\hbar = 1$ reads$^{21-23}$

$$\dot{\rho} = -\hbar \left[ H_{\text{DQD}}, \rho \right] - \int_0^\infty dr tr_{\text{env}} \left[ \left[ V(\tau - r), \rho \otimes \rho_{\text{env}} \right] \right].$$ (2)
where $V(t) = e^{iH_{DQD}t}V e^{-iH_{DQD}t}$ is the coupling operator in the interaction picture and $\tau_{\text{norm}}$ the trace over all bath and lead variables. Generally, Eq. (2) possesses a unique stationary solution which allows us to compute the current.

The numerical solution of the master equation is conveniently performed in the energy eigenbasis of the DQD with the many-body eigenstates $|\xi\rangle$ and the corresponding energies $E_\xi$ and occupation numbers $N_\xi$. The main advantage of this representation is that it brings $V(t)$ to a simple form such that the time integration in Eq. (2) can be evaluated analytically. The direct transitions between the populations are determined by golden-rule rates. For example, tunneling of an electron from a lead to the DQD occurs with a rate $\Gamma_{\text{in}}^{\text{out}} \propto f(E_f - E_i - \mu) + f(E_f - E_i + \mu)$ with $f$ being the Fermi function and $E_\xi$ the energies of the initial and final DQD state, whose difference must be compensated by the energy of the incoming lead electron. Hence, these terms can occur only when $E_f \leq E_i + \mu$. In turn, $\Gamma_{\text{out}}^{\text{in}} \propto f(E_f - E_i + \mu)$, which differs from $\Gamma_{\text{in}}^{\text{out}}$ only by the sign of the chemical potential. For the dissipative transitions, one finds absorption and emission rates that are linked by Boltzmann factors.

Importantly, owing to the relatively small inter-dot tunneling in our system, off-diagonal density matrix elements are rather relevant. Indeed, one observes that eventually becomes a block diagonal in the occupation number $N_\xi$, where the blocks correspond to subspaces with equal DQD occupation $N_\xi$. Within these blocks, however, off-diagonal density matrix elements may have an appreciable size, which implies that a secular approximation is suitable for coherences $\rho_{DQD}$ between states with different occupation numbers.

**Data availability**

The data that support the findings of this study are available from the authors upon reasonable request.

**Code availability**

The computational code used for this study is available from the authors upon reasonable request.

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**References**

1. Xue, X. et al. CMOS-based cryogenic control of silicon quantum circuits. *Nature* 593, 205 (2021).
2. Yang, C. H. et al. Operation of a silicon quantum processor unit cell above one kelvin. *Nature* 580, 350 (2020).
3. Blick, R. H., Pfannkuche, D., Haug, R. J., Klitzing, K. V. & Eberl, K. Formation of a coherent mode in a double quantum dot. *Phys. Rev. Lett.* 80, 4032 (1998).
4. Hayashi, T., Fujisawa, T., Cheong, H. D., Jeong, Y. H. & Hirayama, Y. Coherent manipulation of electronic states in a double quantum dot. *Phys. Rev. Lett.* 91, 226804 (2003).
5. Petta, J. R., Johnson, A. C., Marcus, C. M., Hanson, M. P. & Gossard, A. C. Manipulation of a single charge in a double quantum dot. *Phys. Rev. Lett.* 93, 186802 (2004).
6. Koppen, F. H. L. et al. Control and detection of singlet-triplet mixing in a random nuclear field. *Science* 309, 1346 (2005).
7. Petta, J. R. et al. Coherent manipulation of coupled electron spins in semiconductor quantum dots. *Science* 319, 2180 (2005).
8. Fujisawa, T. et al. Spontaneous emission spectrum in double quantum dot devices. *Science* 282, 932 (1998).
9. Brandes, T. & Kramer, B. Spontaneous emission of phonons by coupled quantum dots. *Phys. Rev. Lett.* 83, 3021 (1999).
10. van der Wiel, W. G. et al. Electron transport through double quantum dots. *Rev. Mod. Phys.* 75, 1 (2002).
11. Hofmann, A. et al. Phonon spectral density in a GaAs/AlGaAs double quantum dot structure. *Phys. Rev. B* 78, 033320 (2009).
12. Vorontsov, S., Mucciolo, E. R. & Baranger, H. U. Phonon decoherence of a double quantum dot charge qubit. *Phys. Rev. B* 71, 205322 (2005).
13. Barthold, P., Hohls, F., Maire, N., Pierz, K. & Haug, R. J. Enhanced shot noise in tunneling through a stack of coupled quantum dots. *Phys. Rev. Lett.* 96, 246804 (2006).
14. Kießlich, G., Scholl, E., Brandes, T., Hohls, F. & Haug, R. J. Noise enhancement due to quantum coherence in coupled quantum dots. *Phys. Rev. Lett.* 99, 206602 (2007).
15. Braggio, A., Flindt, C. & Novotný, T. Non-Markovian signatures in the current noise of a charge qubit. *Phys. E* 40, 1745 (2008).
16. Sánchez, R., Kohler, S., Hänggi, P. & Platero, G. Electron bunching in stacks of coupled quantum dots. *Phys. Rev. B* 77, 035409 (2008).
17. Xie, Q., Madhukar, A., Chen, P. & Kohayashi, N. P. Vertically self-organized InAs quantum box islands on GaAs(100). *Phys. Rev. Lett.* 75, 2542 (1995).
18. Eisele, H. et al. Cross-sectional scanning-tunneling microscopy of stacked InAs quantum dots. *Appl. Phys. Lett.* 75, 106 (1999).
19. Barthold, P., Hohls, F., Maire, N., Pierz, K. & Haug, R. J. Enhanced shot noise in tunneling through coupled self-assembled InAs quantum dots. *Phys. Status Solidi C* 3, 3786 (2006).
20. Hapke-Wurst, I. et al. Tuning the onset voltage of resonant tunneling through InAs quantum dots by growth parameters. *Appl. Phys. Lett.* 82, 1209 (2003).
21. Redfield, A. G. On the theory of relaxation processes. *IBM J. Res. Dev.* 1, 19 (1957).
22. Breuer, H.-P. & Petruccione, F. *Theory of Open Quantum Systems*. (Oxford University Press, 2003).
23. Stark, M. & Kohler, S. Coherent quantum ratchets driven by tunnel oscillations. *Europhys. Lett.* 91, 20007 (2010).
24. Leggett, A. J. et al. Dynamics of the dissipative two-state system. *Rev. Mod. Phys.* 59, 1 (1987).
25. Hänggi, P., Talkner, P. & Borkovec, M. Reaction-rate theory: fifty years after Kramers. *Rev. Mod. Phys.* 62, 251 (1990).
26. Weiss, U. *Quantum Dissipative Systems*, 2nd edn. (World Scientific, 1998).
27. Makhlin, Y., Schön, G. & Shnirman, A. Quantum-state engineering with Josephson-junction devices. *Rev. Mod. Phys.* 73, 357 (2001).
28. Forster, F. et al. Characterization of qubit dephasing by Landau-Zener-Stückelberg-Majorana interferometry. *Phys. Rev. Lett.* 112, 116803 (2014).
29. Bello, M., Platero, G. & Kohler, S. Doubloon lifetimes in dissipative environments. *Phys. Rev. B* 96, 045408 (2017).
30. Hapke-Wurst, I., Zeitler, U., Haug, R. J. & Pierz, K. Mapping the g factor anisotropy of InAs self-assembled quantum dots. *Phys. E* 12, 802 (2002).
31. Krebs, O. et al. Hyperfine interaction in InAs/GaAs self-assembled quantum dots: Anisotropic nuclear polarization versus spin relaxation. *Phys. Rev. B* 97, 045302 (2018).
32. Devoret, M. H. et al. Effect of the electromagnetic environment on the Coulomb blockade in ultrasmall tunnel junctions. *Phys. Rev. Lett.* 64, 1824 (1990).
33. Ingold, G.-L. & Nazarov, Y. V. In *Single Charge Tunneling*, NATO ASI Series B, Vol. 294, p. 21 (eds. Grabert, H. and Devoret, M. H.). (Plenum, 1992).
34. Weiss, U. & Wöllensak, M. Dynamics of the biased two-level system in metals. *Phys. Rev. Lett.* 62, 1663 (1989).
35. Darau, D., Begemann, G., Donarini, A. & Grifoni, M. Interference effects on the transport characteristics of a benzene single-electron transistor. *Phys. Rev. B* 79, 235404 (2009).

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**Author contributions**

O.D. and J.C.B. performed the measurements and the analysis of the experimental data. R.H. and S.K. developed the theoretical model and computed the numerical data. All authors participated in the discussions of the results and contributed to the writing and editing the manuscript. The research was supervised by S.K. and R.J.H.

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**Competing interests**

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**Correspondence**

For materials should be addressed to Olfa Dani.

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