Strong Coupling of a Quantum Oscillator to a Flux Qubit at its Symmetry Point

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A flux qubit biased at its symmetry point shows a minimum in the energy splitting (the gap), providing protection against flux noise. We have fabricated a qubit of which the gap can be tuned fast and have coupled this qubit strongly to an LC oscillator. We show full spectroscopy of the qubit-oscillator system and generate vacuum Rabi oscillations. When the gap is made equal to the oscillator frequency \( \nu_{\text{osc}} \) we find the largest vacuum Rabi splitting of \( \sim 0.1 \nu_{\text{osc}} \). Here being at resonance coincides with the optimal coherence of the symmetry point.

Superconducting qubits coupled to quantum oscillators have demonstrated a remarkable richness of physical phenomena in the last few years. After the first reports of coherent state transfer and strong coupling [1, 2], we have witnessed a rapid development of the field called circuit quantum electrodynamics (CQED) using high quality superconducting oscillators realizing quantum gates [3], algorithms [4] as well as non-classical states of light and matter in artificially fabricated structures [5, 6]. Among the different implementations the transmon [1, 3–5] and the phase qubit [6] dominated this development. With flux qubits the avoided crossing between qubit and oscillator level was observed [1, 8] and the coherent single-photon exchange between qubit and oscillator was demonstrated [8]. However, the coherence of the flux qubit is optimally preserved only in the symmetry point for flux bias, where the energy splitting is minimal. This minimal splitting \( (h \Delta) \) is called the gap and depends (exponentially) on the properties of the Josephson junctions.

Therefore, the gap is hard to control in fabrication and it is impossible to make it coincide with a fixed oscillator frequency. We now have developed a flux qubit of which the gap \( \Delta \) can be tuned over a broad range on sub-ns time scales [9]. With the use of this control we demonstrate strong coupling of a flux qubit with good coherence to a lumped-element LC oscillator, showing fast and long-lived vacuum Rabi oscillations.

Parameters of the superconducting qubits can be to a large extent chosen in the design phase. For strong coupling, where the interaction strength \( g \) exceeds the cavity and qubit loss rates, the rotating-wave approximation (RWA) can be applied and the system can be described by a Jaynes-Cummings type Hamiltonian. If \( g \) approaches the qubit or oscillator frequencies the RWA no longer holds, leading into the ultra-strong coupling regime [10, 11]. For a flux qubit the ratio \( g/\nu_{\text{osc}} \) can be an order of magnitude larger than for charge and phase qubits [12], while these latter devices have a coupling that can be several orders of magnitude larger than the atom-light interaction energy [11]. For good coherence, operating the qubit at its spectral symmetry point is required. Therefore, experimentally combining galvanic coupling of oscillator and flux qubit with this symmetry point operation provides a major step forward in the development of CQED systems. For the flux qubit at the symmetry point the anharmonicity (distance between 2nd and 3rd level relative to qubit splitting) is very high, allowing very fast operation without quantum leakage.

The investigated system is represented in Fig. 1. The flux qubit has a gradiometric topology [9, 13] by having the Josephson junctions that form the qubit symmetrically attached to the circumference loop as shown in Fig. 1(a,b); this loop is also employed to trap fluxoids (or \( 2\pi \)-phase-winding numbers) [13]. To obtain a tunable-gap qubit the two center junctions form a SQUID structure, where the flux \( f_c \Phi_0 \) \textit{in situ} sets the effective

![FIG. 1: (color online). (a) Circuit schematics: the tunable gap flux qubit (green) coupled to a lumped element superconducting LC oscillator (red) and controlled by the bias lines \( I_c, I_{\text{osc}}, I_a \) (black). The SQUID (blue) measures the state of the qubit. The gradiometer loop (emphasized by a dashed line) is used to trap fluxoids. (b) Scanning Electron Micrograph (SEM) of the sample. (c) Energy diagram of the qubit-oscillator system. The minimum of energy splitting of the qubit \( \Delta \) is reached at the symmetry point when one fluxoid is trapped in the gradiometer loop and the difference in magnetic fluxes \( f_c \Phi_0 \) is 0 controlled by \( I_c \) and \( I_{\text{osc}} \). By controlling the flux \( f_c \Phi_0 \) with \( I_a \) and uniform field \( B \) one can tune \( \Delta \) in resonance with oscillator frequency \( \nu_{\text{osc}} \).](attachment:image)
critical current and in this way the qubit gap $\Delta$ [9]. The gap covers nearly two decades from 150 MHz to 12 GHz, providing full frequency control relative to the oscillator at 2.723 GHz (see Fig. 1(c)). The Hamiltonian of the flux qubit can be written as $H_{\text{qubit}} = -\hbar(\epsilon_\sigma + \Delta_\sigma)/2$, where $\sigma_\sigma$ and $\sigma_z$ are Pauli matrices written in the persistent current states basis; $h$ is the magnetic energy bias $h(e\sigma + \Delta\sigma)/2$, where $e\sigma$ and $\Delta\sigma$ are the circulating current in the qubit and $2e\sigma$ being the circulating current of the qubit eigenstates and a long relaxation time $\tau_{\text{rel}}$, gradually increasing from $T_1 = 1$ s to $T_1 = 4$ s at $\nu_{\text{osc}} = 9$ GHz. In the second step we applied a square current pulse in $I_q$, tuning $\nu_{\text{qubit}}$ to the required frequency, combined with a microwave (MW) excitation. After each excitation pulse the qubit was returned to $\nu_{\text{qubit}} = 9$ GHz and a short bias current pulse $I_0$ was applied to the SQUID for measurement of the qubit state [15].

By measuring the qubit away from its symmetry point we benefit from the high expectation value of the circulating current of the qubit eigenstates and a long relaxation time $T_1$, gradually increasing from $T_1 = 1.5$ $\mu$s in the symmetry point to $T_1 > 4$ $\mu$s at $\nu_{\text{qubit}} = 9$ GHz with $\Delta \approx 2$ GHz.

Figure 2(c) shows the spectrum of the system for $\Delta < \nu_{\text{osc}}$. In order to be resonant with the oscillator the qubit has to be tuned away from its symmetry point. The clear observation of the level anti-crossing with the largest level splitting of 180 MHz (vacuum Rabi splitting) confirms that the system is in the strong eQED regime. To observe the spectral line of the oscillator we use a Landau-Zener transition at the anti-crossing of the qubit and oscillator energies. A passage through the anti-crossing region performed with a dc-shift pulse on $I_q$ with

![Diagram of Landau-Zener transitions transferring the excitation of the oscillator to the qubit. (c) MW frequency vs $f_0$. A black dotted line is obtained from Eq. (1) with $\nu_{\text{qubit}} = 9$ GHz (see Fig. 1(c)). The oscillator is coupled to the qubit via the same shared part of the wire with the qubit-SQUID mutual inductance $M \approx 5.5$ pH (since $M$ is much smaller than the Josephson inductances of the SQUID junctions most of the current flows through the shared part). Unlike the plasma resonance of the SQUID the connections of the oscillator to the external circuit occurs in the voltage nodes of the resonance mode. Thus the oscillator quality factor $Q$ is not severely affected by the external impedance, reaching $Q \sim 6000$ for strong excitation and a few hundreds at low photon number. Being designed as part of the readout circuit, it was not optimized for high $Q$ performance.

All structures excluding the bottom plate of the capacitors $C$ were fabricated in the same layer of aluminum using standard lithography techniques [15]. The bottom plates of the capacitors were fabricated in a separate layer followed by a plasma oxidation step resulting in a thin layer of Al-AlO$_x$-Al used as the dielectric of the capacitor. The experiment was conducted in a dilution refrigerator at its base temperature of 20 mK.

The interaction between the qubit and the oscillator can be described by $H_{\text{int}} = h\nu_\sigma(a + a^\dagger)\sigma_z$ written in the basis of the persistent current states, where $g = MI_qI_0$ is the coupling strength, $I_0 = \sqrt{\hbar\nu_{\text{osc}}/(4I)}$ is the measure for zero-point current fluctuations, $\nu_\sigma$ is defined as $\nu_\sigma = (\cos \eta \sigma_x - \sin \eta \sigma_z) \sigma_z$, $\nu_{\text{osc}} = 2\nu_{\text{qubit}}$, $\nu_{\text{osc}} = h\nu_{\text{osc}}/\hbar$, and $\nu_{\text{qubit}} = h\nu_{\text{qubit}}/\hbar$ in the symmetrically-split $I_q$ line, acting on the qubit flux $\Phi_\Phi$. Similarly, the line $I_0$ together with the homogeneous field $B$ generated by an external coil, modulates $\Phi_\Phi$ and changes $\Delta$. The structural symmetry suppresses crosstalk, implying a fully selective control.

The qubit states are detected with a dc-SQUID which is coupled to the qubit with a shared part of a wire of length $l = 6$ $\mu$m, width $w = 350$ nm, and thickness $t = 70$ nm leading to a mutual qubit-SQUID inductance $M \approx 5.5$ pH. Half of $M$ is provided by a kinetic inductance of the shared part $\nu_{\text{osc}} = 1/(2\sqrt{2L(C/2)}) = 2.723$ GHz. The oscillator is coupled to the qubit via the same shared part of the wire with the qubit-SQUID mutual inductance $M \approx 5.5$ pH (since $M$ is much smaller than the Josephson inductances of the SQUID junctions most of the current flows through the shared part). Unlike the plasma resonance of the SQUID the connections of the oscillator to the external circuit occurs in the voltage nodes of the resonance mode. Thus the oscillator quality factor $Q$ is not severely affected by the external impedance, reaching $Q \sim 6000$ for strong excitation and a few hundreds at low photon number. Being designed as part of the readout circuit, it was not optimized for high $Q$ performance.

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a rise time of 4 ns is found to lead to $\sim 25\%$ probability of an oscillator photon to be converted to the excited state of the qubit. The latter can be detected by the SQUID and the oscillator line becomes visible on spectrum.

The sequence of operations to observe the vacuum Rabi oscillations starts by tuning the qubit gap $\Delta$ into the vicinity of $\nu_{osc}$, setting $f_\alpha$ by the external magnetic field. The qubit is tuned to $\nu_{qb} = 7$ GHz by $f_\epsilon$, and a $\pi$-pulse is applied to excite the qubit. Subsequently, the qubit is taken to the symmetry point by means of a fast 0.3 ns rise time pulse. As the qubit energy changes fast relative to the coupling strength $g$, this transfer is non-adiabatic. The qubit is kept here for a time $\Delta t$, then returned fast to the 7 GHz level and finally read out. While the qubit is in the symmetry point, qubit and oscillator coherently exchange the excitation with a frequency that is determined by the coupling and the detuning $\delta \nu = \Delta - \nu_{osc}$ according to Eq. (2)

$$
\nu_R \equiv \sqrt{4g^2 + \delta \nu^2}.
$$

The vacuum Rabi oscillations are shown in Fig. 3(a). For each value of $f_\alpha$ (and therefore $\Delta$), the probability to find the qubit in one of its eigenstates oscillates as a function of $\Delta t$ with a frequency that is minimal for $f_\alpha \approx -0.292$, the point where $\Delta = \nu_{osc}$. Fig. 3(b) shows the spectrum as a function of $f_\alpha$, with the avoided crossing clearly visible. From the slope the value $d\Delta/df_\alpha \approx 69.5$ GHz/m$\Phi_0$ can be determined, which is used to estimate $\delta \nu$ as $\delta \nu = (d\Delta/df_\alpha)df_\alpha$. By fitting to Eq. (2) the bare coupling $2g$ is found to be 239 MHz.

We now focus on the most interesting on-resonance regime with $\Delta = \nu_{osc}$. From [1] one can see that here the qubit-oscillator coupling is fully transversal $\eta = \pi/2$, making the effective coupling attain its maximum value $g$. The measurement of the spectrum, shown in Fig. 4(a), indeed exhibits the maximum vacuum Rabi splitting of 239 MHz corresponding to the highest photon exchange rate between oscillator and qubit.

Interestingly, Landau-Zener transitions now change qualitatively: after the passage through the anti-crossing the energy of the state $|0\rangle$ remains higher than that for $|g1\rangle$ making the qubit and the oscillator almost fully exchange their populations and creating strong asymmetry in the visibility of the spectral lines in Fig. 4(a) (for $\Delta < \nu_{osc}$, see Fig. 2(b,c) where the qubit and the oscillator tend to retain their populations).

In Fig. 4(b) we demonstrate vacuum Rabi oscillations for different $f_\epsilon$. Taking into account only $|0, 1\rangle$ oscillator states the Rabi frequency can be found analytically from $[1]$ as

$$
\nu_R = \left(4g^2 + \nu_{osc}^2 + \nu_{qb}^2 - 2\sqrt{4g^2\nu_{qb}^2 + \nu_{osc}^2}\nu_{osc}\right)^{1/2},
$$

which explains the measured data as shown in Fig. 4(c). Note that Eq. (4) reduces to Eq. (2) if $\epsilon = 0$.

Implementation of the gap control loop might in principle lead to additional decoherence. However, in practice the effect of flux noise in $\alpha$-loop in our design is estimated to be about two orders of magnitude smaller than that of the $\epsilon$-loop. Measuring the qubit in the symmetry point we found $T_2 \simeq 300$ ns and $T_1 \simeq T_{Rabi} \simeq 1.5 \mu$s for $\Delta \sim 1.5 - 6$ GHz. While $T_1$ and $T_{Rabi}$ are in accordance with design values we observed no dependence of $T_2 < 2T_1$ on $\Delta$ which rules out flux noise in both $f_\epsilon$, $f_\alpha$ as a limiting decoherence source in the symmetry point [17].

Since the qubit is optimally protected from low-frequency flux noise in the symmetry point the vacuum Rabi oscillations show the longest decay time of $\sim 40$ ns. This is limited only by the losses in the oscillator, as...
two representative cases: the gap was tuned substantially below and in resonance with the oscillator frequency. For the particularly interesting case of $\Delta = \nu_{osc}$ the qubit reaches the resonance conditions in its symmetry point thus combining the two most desired ingredients of the cQED regime: strong coupling and optimal coherence. Here the avoided level crossing attains its maximal value of $2g \approx 0.09 \cdot \nu_{osc}$ and at the same time the qubit is effectively protected from 1/f flux noise resulting in the longest and fastest sequence of on-resonant vacuum Rabi oscillations. The interaction strength can be readily increased reaching the ultra-strong regime $g \sim \{\nu_{osc}, \nu_{qb}\}$.

We thank P. C. de Groot and R. N. Schouten for useful discussions. This work was supported by the Dutch NanoNed program, the Dutch Organization for Fundamental Research (FOM), and the EU projects EuroSQIP and CORNER.

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FIG. 4: (color online). (a) MW frequency vs $f_\phi$. The dotted white line is obtained from Eq. (1) with $I_p = 400$ nA and $\Delta = \nu_{osc}$. The observed vacuum Rabi splitting is maximal due to fully transverse coupling of the qubit to the oscillator $\eta = \pi/2$. (b) Vacuum Rabi oscillations for different values of $f_\phi$. In the experiment $f_\phi$ was controlled by the amplitude of the current pulse $I$, while $\Delta$ was tuned to $\nu_{osc}$ by changing the external magnetic field $B$. The inset shows $\nu_R$ extracted from data (red circles) and estimated from Eq. (3) (blue line). The color indicates the switching probability of the SQUID minus 0.5.

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measured coherence times of the qubit at the symmetry point are much longer [16]. Out of the symmetry point we measure the usual rapid degradation of the qubit coherence to $T_2 \sim 15 - 20$ ns for $\epsilon \gg \Delta$ [15] due to flux noise which precludes generation of long-living vacuum Rabi oscillations. Obviously, by using a fully compatible fabrication technology optimized for high $Q$ oscillators [11, 13-15] it is possible to achieve a ratio of $g/\max(T_2^{-1}, T_1^{-1}, 2\nu_{osc}/Q) > 100$ necessary for creating qubit-oscillator entanglement with high fidelity.

In summary, we experimentally studied a tunable gap flux qubit coupled galvanically to a superconducting lumped-element LC oscillator. We measured the avoided level crossings and generated vacuum Rabi oscillations for two representative cases: the gap was tuned substantially below and in resonance with the oscillator frequency. For the particularly interesting case of $\Delta = \nu_{osc}$ the qubit reaches the resonance conditions in its symmetry point thus combining the two most desired ingredients of the cQED regime: strong coupling and optimal coherence. Here the avoided level crossing attains its maximal value of $2g \approx 0.09 \cdot \nu_{osc}$ and at the same time the qubit is effectively protected from 1/f flux noise resulting in the longest and fastest sequence of on-resonant vacuum Rabi oscillations. The interaction strength can be readily increased reaching the ultra-strong regime $g \sim \{\nu_{osc}, \nu_{qb}\}$. We thank P. C. de Groot and R. N. Schouten for useful discussions. This work was supported by the Dutch NanoNed program, the Dutch Organization for Fundamental Research (FOM), and the EU projects EuroSQIP and CORNER.

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[1] A. Wallraff et al., Nature 431, 162 (2004).
[2] I. Chiorescu et al., Nature 431, 159-162 (2004).
[3] J. Majer et al., Nature 449, 443 (2007).
[4] L. Di Carlo et al., Nature 460, 230 (2009).
[5] J. M. Fink et al., Nature 454, 315-318 (2008).
[6] M. Hofheinz et al., Nature 459, 546 (2009).
[7] E. Il’ichev et al., Phys. Rev. Lett. 91, 097906 (2003). A. A. Abdumalikov, O. Astafiev, Y. Nakamura, Y. A. Pashkin, and J. S. Tsai, Phys. Rev. B 78, 180502(R) (2008). F. Deppe et al., Nat. Phys. 4, 686 (2008).
[8] J. Johansson et al., Phys. Rev. Lett. 96, 127006 (2006).
[9] F. G. Paauw, A. Fedorov, C. J. P. M Harmans, and J. E. Mooij, Phys. Rev. Lett. 102, 090501 (2009).
[10] J. Hausinger and M. Grifoni, New J. Phys. 12, 032109 (2009). B. Peropadre, P. Forn-Díaz, E. Solano, Y. A. Pashkin, and J. S. Tsai, Phys. Rev. B 78, 180502(R) (2008). F. Deppe et al., Nat. Phys. 4, 686 (2008).
[11] F. Deppe et al., arXiv:1005.1559 (2010).
[12] Assuming galvanic and capacitive couplings for flux and oscillators [11, 13-15] it is possible to achieve a ratio of $g/\max(T_2^{-1}, T_1^{-1}, 2\nu_{osc}/Q) > 100$ necessary for creating qubit-oscillator entanglement with high fidelity. In summary, we experimentally studied a tunable gap flux qubit coupled galvanically to a superconducting lumped-element LC oscillator. We measured the avoided level crossings and generated vacuum Rabi oscillations for two representative cases: the gap was tuned substantially below and in resonance with the oscillator frequency. For the particularly interesting case of $\Delta = \nu_{osc}$ the qubit reaches the resonance conditions in its symmetry point thus combining the two most desired ingredients of the cQED regime: strong coupling and optimal coherence. Here the avoided level crossing attains its maximal value of $2g \approx 0.09 \cdot \nu_{osc}$ and at the same time the qubit is effectively protected from 1/f flux noise resulting in the longest and fastest sequence of on-resonant vacuum Rabi oscillations. The interaction strength can be readily increased reaching the ultra-strong regime $g \sim \{\nu_{osc}, \nu_{qb}\}$. We thank P. C. de Groot and R. N. Schouten for useful discussions. This work was supported by the Dutch NanoNed program, the Dutch Organization for Fundamental Research (FOM), and the EU projects EuroSQIP and CORNER.

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[3] J. Majer et al., Nature 449, 443 (2007).
[4] L. Di Carlo et al., Nature 460, 230 (2009).
[5] J. M. Fink et al., Nature 454, 315-318 (2008).
[6] M. Hofheinz et al., Nature 459, 546 (2009).
[7] E. Il’ichev et al., Phys. Rev. Lett. 91, 097906 (2003). A. A. Abdumalikov, O. Astafiev, Y. Nakamura, Y. A. Pashkin, and J. S. Tsai, Phys. Rev. B 78, 180502(R) (2008). F. Deppe et al., Nat. Phys. 4, 686 (2008).
[8] J. Johansson et al., Phys. Rev. Lett. 96, 127006 (2006).
[9] F. G. Paauw, A. Fedorov, C. J. P. M Harmans, and J. E. Mooij, Phys. Rev. Lett. 102, 090501 (2009).
[10] J. Hausinger and M. Grifoni, New J. Phys. 11, 115015 (2008). J. Bourassa et al., Phys. Rev. Lett. 102, 090501 (2009).
[11] J. Hausinger and M. Grifoni, New J. Phys. 10, 115015 (2008). J. Bourassa et al., Phys. Rev. A 80, 032109 (2009). B. Peropadre, P. Forn-Díaz, E. Solano, J. J. Garcia-Ripoll, arXiv:0912.3456 (2009). S. Ashhab, and F. Nori, arXiv:0912.4888 (2009). T. Niemczyk et al., arXiv:1003.2376 (2010).
[12] F. P. Díaz-Pérez et al., arXiv:1005.1559 (2010).
[13] Assuming galvanic and capacitive couplings for flux and phase qubits, respectively, the ratio $g/\nu_{osc}$ for a flux qubit can be $\phi I_{rms}/(\langle \phi \rangle^2 / 2 \nu_{rms}) = 0.25R_K/\nu \approx 10$ times larger. Here $\epsilon$ is a charge of an electron, $R_K$ a quantum of resistance, $\nu$ is the characteristic impedance of the oscillator and $\langle \phi \rangle$ is a number of charge states.
[14] R. H. Koch et al., Phys. Rev. Lett. 96, 127001 (2006).
[15] J. Majer, J. Butcher, and J.E. Mooij, Appl. Phys. Lett. 80, 3638 (2002).
[16] P. Bertet et al., Phys. Rev. Lett. 95, 257002 (2005).
[17] P. Lambropoulos, D. Petsymay, Fundamentals of Quantum Optics and Quantum Information, Springer, Berlin, (2007).
[18] Detailed analysis of decoherence of the tunable flux qubit will be published elsewhere.
[19] F. Yoshihara et al., Phys. Rev. Lett. 97, 167001 (2006). K. Kakuyanagi et al., Phys. Rev. Lett. 98, 047004 (2007).