Study on design, manufacture, and cutting performance of circular-arc milling cutters for machining titanium alloy

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Abstract
Titanium alloy is widely used for manufacturing structural parts of high-end equipment due to its excellent mechanical properties, despite difficulty in being machined. Nowadays, titanium alloy parts are mostly machined by ball-end milling cutters (BEMC), but the cutting edge structure of the BEMC limits the improvement in machining efficiency and surface quality of the parts. In this paper, a circular-arc milling cutter (CAMC) with large-curvature cutting edge was proposed; the differential geometry method was used for establishing the geometric model for the contour surface of the CAMC and the mathematical model for the spiral cutting edge line; the conversion matrix between grinding wheel and workpiece coordinates was introduced to derive the equation of grinding wheel trajectory when the rake face of the CAMC was ground; the self-designed CAMC was ground and tested in accuracy. The comparative research was conducted experimentally on the side milling of titanium alloy TC4 with the CAMC and BEMC, and consequently the variation laws of milling forces, wear morphology, and machined surface quality were obtained about the two types of milling cutters. The results indicated that the CAMC can effectively reduce the main milling force and keep the milling process stable. Moreover, the CAMC was worn slower and produced better surface quality than the BEMC.

Keywords
Titanium alloy TC4 · Circular-arc milling cutter · Design and manufacture of milling cutters · Wear morphology · Surface quality

1 Introduction
Titanium alloy has become a preferable material for key parts in the aerospace industry due to its merits such as high strength, strong corrosion resistance, and low-temperature performance [1, 2]. Cutting tools meet new challenges as the manufacture of high-end equipment makes an increasing demand on the machining quality and efficiency of titanium alloy components. Nowadays, the frequently used ball-end milling cutters (BEMC) have large-curvature cutting edge and thus tend to shrink milling step to ensure good machined surface quality, but this decreases the efficiency of machining titanium alloy and meanwhile increases the manufacturing cost more or less [3, 4]. Therefore, it is essential and urgent to improve the efficiency of milling titanium alloy for its better application and promotion.

In designing processing tools for titanium alloy, Chen et al. [5] presented a new mathematical model for S-shaped edge curve. The model overcomes the complex computation and poor adaptability of the traditional modeling method and enhances the cutting efficiency and stability of BEMC. Masahiko et al. [6] developed successfully two types of BEMC with a unique cutting edge and verified experimentally that a high finishing accuracy and minor cutting forces were realized by the above-mentioned cutting tools. Engin et al. [7] established a generalized mathematical model of most helical end milling cutters and verified correctness of the model by the experiment on milling titanium alloy. Altinta et al. [8, 9] presented a generalized mathematical model for most helical end milling cutters and solved the problems of chatter vibrations, torque and power constraints, and dimensional form errors. Li et al. [10] presented a barrel-ball milling cutter for blisk machining, and proposed the selection of cutter parameter and calculation of cutter location.

Many scholars have researched the trajectory and posture of grinding wheel and novel methods for grinding. Ren et al.
[11] proposed a novel method of five-axis flute grinding based on the theories of analytic geometry and envelope and verified the validity of the method by 3D simulations and machining experiments. The results show that this grinding method can effectively reduce the errors in grinding helical flutes. Pham et al. [12] proposed a manufacturing model of flat-end milling cutters using a five-axis computer numerical control grinding machine, based on the research into a given wheel profile and the relative movements between workpiece and grinding wheel. The model was practical and efficient for the manufacture of an end milling cutter. Wang et al. [13] generated a model of grinding wheel trajectory for machining helical grooves in terms of the grinding wheel’s position and orientation and provided a new approach for flute grinding of end milling cutters. Chen et al. [14] proposed new mathematical models and grinding methods of BEMC based on the orthogonal spiral cutting edge curve. It was found through the grinding experiments that both rake face with equal rake angle and flank face with equal clearance angle improve effectively chip removal conditions and machining performance of BEMC. Li et al. [15] reported a graphical analysis method to obtain the structural parameters and geometric shapes of helical grooves. Based on this, the influence of the geometry and grinding parameters of grinding wheels was discussed on radial rake angles, groove width, and core radius. Tang et al. [16] proposed three practical and reliable grinding methods based on the research into mathematical models of spiral grooves, conical flank, and cutter clearance and verified experimentally reliability of the proposed grinding methods. Chen et al. [17] presented a novel method to grind the rake face of a taper BEMC using a CBN spherical grinding wheel. This method used the self-adaptation characteristics of a sphere to decrease the number of simultaneous cooperative axes of the CNC tool grinder from 5 to 4. This boosted the grinding accuracy of rake faces. Chen et al. [18] carried out research on the design and manufacturing of new concave-arc ball-end milling cutters. By computing the radial and axial cutting speeds of the grinding wheel, an ideal geometric profile accuracy of milling cutters was obtained.

To sum up, the overall research into the milling cutters for machining titanium alloy mostly focuses on the designing, grinding and cutting performance of BEMC [19–22]. Nowadays, some companies such as Walter and Fraisa have proposed a few novel cutting tools for machining titanium alloy, such as NB-NVDS and MC230 Advance. The novel cutters partly increase the curvature of side cutting edge through reducing the edge radius of ball end and thus enhance side milling efficiency. Nonetheless, smaller radius of bottom edge increases grinding difficulty and decreases overall tool rigidity. Consequently, combined with the design idea for integration of tool design and manufacture [23], this paper employed the differential geometry method for designing a circular-arc milling cutter (CAMC) with large curvature, resolving the contradiction of the above novel cutters between edge radius of ball end and overall tool rigidity. This provides a new idea and method for the design and manufacture of milling cutters for machining titanium alloy.

### 2 Design of CAMC

#### 2.1 Presentation of tool structure and establishment of geometric model

The CAMC designed in this paper is a rotary tool. The tool contour can be obtained by rotating the generatrix around the rotation axis. Figure 1 shows the generatrix of the CAMC in the $X_0OZ_0$ coordinates. The generatrix consists of end cutting edge $AB$, transitional arc $BC$, and circumferential cutting edge $CD$. The two parts of cutting edge are connected by the transitional arc. $R_1$ stands for the arc radius of generatrix $AB$ at the end cutting edge, and its circle center is expressed as $O_1$. $R_2$ stands for the arc radius of the generatrix at the circumferential cutting edge, and its circle center is expressed as $O_2$. The radius of transitional cutting edge $BC$ is expressed as $r$, and its circle center $O_3$. In order to ensure that each section of the arc is tangent and the arc radius of the transitional cutting edge

![Figure 1. Generatrix of the CAMC](image-url)
is reduced, the arc radius of circumferential cutting edge CD can be 4–12 times as long as that of the tool shank.

Here, the equation for the generatrix of end cutting edge AB is expressed as follows:

\[
\begin{align*}
x(u) &= R_1 \sin \left( \frac{u}{R_1} \right) \\
z(u) &= \sqrt{R_1^2 - \left( R_1^2 - d_1^2 \right)} - R_1 \cos \left( \frac{u}{R_1} \right) \\
&= C_2 + R_1 \cos \left( \frac{u}{R_1} \right) \\
0 &\leq u \leq k_1
\end{align*}
\] (1)

In the above equation, \( u \) stands for the arc length from starting point A to any point on the generatrix AD and has a value range of \( 0 \leq u \leq k_1 \).

Here are the equations for the generatrix of circumferential cutting edge CD:

\[
\begin{align*}
x(u) &= R_2 \sin \left( \frac{u-k_1 + k_2}{R_2} \right) - \left( R_2 - d_2 \right) \\
z(u) &= R_2 - R_1 \cos \left( \frac{d_1}{R_1} \right) - R_2 \cos \left( \frac{u-k_1 + k_2}{R_2} \right) \\
&\quad + (0.5\pi R_2 - k_2) \\
0 &\leq u \leq k_1
\end{align*}
\] (2)

where \( k_1 \) and \( k_2 \) are respectively expressed as follows:

\[
\begin{align*}
k_1 &= R_1 \arcsin \left( \frac{d_1}{R_1} \right) \\
k_2 &= R_2 \arcsin \left( \frac{d_1}{R_2} \right) \\
&\quad - \left( R_2 - d_1 \right)
\end{align*}
\] (3)

Figure 2 displays the rotational contour of the CAMC in the coordinate system \( O(X_0Y_0Z_0) \). \( Z_0 \) stands for the rotational axis. The equation for the rotational contour surface of the CAMC is expressed as follows:

\[
\begin{bmatrix}
x(u) \cos(\varphi) \\
x(u) \sin(\varphi) \\
z(u) \\
1
\end{bmatrix}
\] (4)

In the above equation, \( \varphi \) refers to the angle rotating around \( Z_0 \) axis. The mathematical model for the structural contour surface of the CAMC is obtained by putting Eqs. (1) and (2) into Eq. (4). In order to facilitate the subsequent coordinate transformation of grinding wheel, the fourth row of the calculated pose matrix is set as 1. Here, the mathematical model for the generatrix of end cutting edge AB goes as follows:

\[
\begin{bmatrix}
x(u) \cos(\varphi) \\
x(u) \sin(\varphi) \\
z(u) \\
1
\end{bmatrix}
\] (5)

The mathematical model for the structural contour surface of circumferential cutting edge generatrix CD is expressed in the following:

\[
\begin{bmatrix}
R_1 \sin \left( \frac{u}{R_1} \right) \\
R_1 \sin \left( \frac{u}{R_1} \right) \\
R_2 \cos \left( \frac{u-k_1 + k_2}{R_2} \right)
\end{bmatrix}
\] (6)

The lead of the equal-lead edge curve of the CAMC is expressed in \( p \). When a point on the edge line passes the rotational angle \( d\varphi \) of the tool shaft, the axial movement distance is equal to the product of the partial derivative of the edge line equation \( r \) to \( u \) and the generatrix distance differential variable \( du \), expressed as follows:

\[
pd\varphi = \frac{\partial r}{\partial u} du
\] (7)

The expression of the equal-lead edge curve of the CAMC is obtained by integrating Eq. (7), as shown below:

\[
\varphi(u) = \frac{1}{p} \sqrt{(x')^2 + (z')^2}du + \varphi_C
\] (8)

\( \varphi_C \) stands for the constant of integration, \( \varphi_C = 0 \). The equation for the edge curve of the CAMC is derived from simultaneous Eqs. (1), (2), (4), (5), and (8).

The equation for the edge curve of the CAMC is expressed as follows:
The following is the equation for the circumferential edge curve of the CAMC:

\[
\begin{align*}
\mathbf{r}_{AC} &= \left[ \begin{array}{c}
R_1 \sin \left( \frac{u}{R_1} \right) \\
R_1 \cos \left( \frac{u}{R_1} \right) \\
1 + C_2 + R_1 \cos \left( \frac{u}{p} \right)
\end{array} \right] \\
\mathbf{r}_{CD} &= \left[ \begin{array}{c}
R_2 \sin \left( \frac{u-k_1 + k_2}{R_2} \right) - (R_2-d_z) \cos \left( \frac{u}{p} \right) \\
R_2 \cos \left( \frac{u-k_1 + k_2}{R_2} \right) - (R_2-d_z) \sin \left( \frac{u}{p} \right) \\
-1 + R_2 \cos \left( \arccos \frac{d_1}{R_1} \right) - R_2 \cos \left( \frac{u-k_1 + k_2}{R_2} \right)
\end{array} \right]
\end{align*}
\]  

(9)

The normal plane \( P_n \) is defined as the normal plane \( \mathbf{n} \) of the rake face and base plane \( \mathbf{n} \) of the flank face of the CAMC. In the figure, the base plane is set as \( P_b \), the normal plane \( P_n \), and the cutting plane \( P_c \). The normal rake angle \( \gamma_n \) is defined as the angle between rake face \( P_f \) and base plane \( P_b \), measured on the normal plane \( P_n \). \( N_f(n_1, n_2, n_3) \) stands for the unit normal vector of the rake face and \( N_b(n_1, n_2, n_3) \) the one of the flank face.

The following equation is derived from the geometric angle relationship between the rake face and the base plane of the CAMC:

\[
\begin{align*}
&\frac{1}{1 + \left( \sin \left( \frac{\pi}{R_1} \right) \right)^2} \left[ n_1 \left[ \cos \left( \frac{u}{R_1} \right) \cos \left( \frac{u}{p} \right) - \frac{R_1}{p} \sin \left( \frac{u}{R_1} \right) \sin \left( \frac{u}{p} \right) \right] \\
&+ n_2 \left[ \cos \left( \frac{u}{R_1} \right) \sin \left( \frac{u}{p} \right) + \frac{R_1}{p} \sin \left( \frac{u}{R_1} \right) \cos \left( \frac{u}{p} \right) \right] + n_3 \sin \left( \frac{u}{R_1} \right) \right] = 0
\end{align*}
\]  

(11)

\[
\cos(\gamma_n) = -\mathbf{N}_f \cdot \mathbf{N}_b
\]

\[
= \frac{1}{\sqrt{1 + \left( \sin \left( \frac{\pi}{R_1} \right) \right)^2}} \left[ -n_1 \left[ \sin \left( \frac{u}{p} \right) - \frac{R_1}{p} \sin \left( \frac{u}{R_1} \right) \cos \left( \frac{u}{R_1} \right) \cos \left( \frac{u}{p} \right) \right] \\
+ n_2 \left[ \cos \left( \frac{u}{p} \right) + \frac{R_1}{p} \sin \left( \frac{u}{R_1} \right) \cos \left( \frac{u}{R_1} \right) \sin \left( \frac{u}{p} \right) \right] - \frac{R_1}{p} \sin \left( \frac{u}{R_1} \right) \right]
\]  

(12)

\[
n_1^2 + n_2^2 + n_3^2 = 1
\]  

(13)

The normal vector of the rake face \( \mathbf{N}_f(n_1, n_2, n_3) \) is obtained by solving simultaneous Eqs. (11), (12), and (13).

### 3 Manufacture and detection of the CAMC

#### 3.1 Establishment of grinding model for the CAMC

For the establishment of the mathematical model for the grinding trajectory of the CAMC, the coordinates of any point in the grinding wheel coordinate system are needed to be converted to the workpiece coordinate system. Then the normal vector of the central point in grinding wheel was derived, based on the equations for edge curve as well as the relative position relationship between grinding wheel and workpiece. Furthermore, the mathematical model for grinding wheel

![Diagram](image_url)

**Figure 3.** Simulation of the equal-lead edge curve of the CAMC. (a) \( p = 8 \text{ mm} \). (b) \( p = 12 \text{ mm} \). (c) \( p = 16 \text{ mm} \)
position was deduced in milling. As is shown in Figure 5, in any position, the grinding wheel coordinate system \( O_g \)—\( X_g, Y_g, Z_g \) was first moved parallel along the \( X_g, Y_g, \) and \( Z_g \) axes and then rotated respectively around the \( X_g, Y_g, \) and \( Z_g \) axes. Here, the translational distance is respectively expressed as \( a_x, a_y, \) and \( a_z \) and the rotational angles \( \varphi_x, \varphi_y, \) and \( \varphi_z \).

The conversion matrix from grinding wheel to workpiece coordinates is expressed as follows:

\[
A_g^{-1} = \begin{bmatrix}
\Delta_1 C_{\varphi_y} & \Delta_1 S_{\varphi_y} C_{\varphi_z} + \Delta_2 C_{\varphi_x} & \Delta_1 S_{\varphi_y} S_{\varphi_z} - \Delta_2 S_{\varphi_x} & \Delta_2 S_{\varphi_y} + \Delta_2 S_{\varphi_x} \\
\Delta_2 S_{\varphi_y} & \Delta_2 C_{\varphi_y} C_{\varphi_z} - \Delta_1 C_{\varphi_x} & \Delta_2 C_{\varphi_y} S_{\varphi_z} + \Delta_1 S_{\varphi_x} & \Delta_1 C_{\varphi_y} S_{\varphi_z} + \Delta_1 S_{\varphi_x} \\
-S_{\varphi_y} & C_{\varphi_y} & 0 & 1 \\
0 & 0 & C_{\varphi_z} & 0
\end{bmatrix}
\]

(14)

In the above equation, \( S, C, \Delta_1, \) and \( \Delta_2 \) are respectively abbreviations for \( \sin(\varphi), \cos(\varphi), \cos(\varphi + \varphi_z), \) and \( \sin(\varphi + \varphi_z) \).

The coordinates of the rotational contour surface of grinding wheel were put into the conversion matrix for calculation. For convenience of calculation, the fourth line of the position matrix is set as 1, and then the position matrix of the rotational contour surface of grinding wheel is derived in the workpiece coordinates, as shown below:

\[
\begin{bmatrix}
x(h) \cos(v) \\
x(h) \sin(v) \\
z(h) \\
1
\end{bmatrix} = \begin{bmatrix}
\frac{x(h) \cos(v)}{\Delta_1 C_{\varphi_y} S_{\varphi_z} + \Delta_1 S_{\varphi_y} + \Delta_1 S_{\varphi_x} + \Delta_2 S_{\varphi_z} + \Delta_2 S_{\varphi_x} + \Delta_2 S_{\varphi_z}} \\
\frac{x(h) \sin(v)}{\Delta_2 C_{\varphi_y} S_{\varphi_z} - \Delta_1 C_{\varphi_x} + \Delta_2 C_{\varphi_z} - \Delta_1 S_{\varphi_x} + \Delta_2 S_{\varphi_z} + \Delta_2 S_{\varphi_x}} \\
z(h) \\
1
\end{bmatrix}
\]

(15)

In the equation, \( h \) stands for the length of the grinding wheel generatrix and \( v \) the angle of the grinding wheel generatrix rotating around the \( Z_g \) axis. \( k_3, k_4, \) and \( k_5 \) are all relevant parameters.
parameters of the rotational surface of grinding wheel. Their expressions are specifically as follows:

\[ k_3 = x(h)\cos(v) \quad k_4 = x(h)\sin(v) \quad k_5 = z(h) \]

The unit normal vector \( \mathbf{n}_{og} \) of the central point \( O_g \) in grinding wheel is expressed in the workpiece coordinates as follows:

\[
\mathbf{n}_{og} = \mathbf{A}_g \cdot \frac{1}{\sqrt{x'(h)^2 + z'(h)^2}} \begin{bmatrix} z'(h)\cos(v) \\ z'(h)\sin(v) \\ -x'(h) \end{bmatrix}
\]

\[
= \begin{bmatrix} -z'(h)C\phi_y S\phi_z \Delta_1 - z'(h)S\phi(v) \left[ S\phi_y S\phi_z \Delta_1 - C\phi_z \Delta_2 \right] \\ +x'(h) \left[ S\phi_y S\phi_z \Delta_1 + C\phi_z \Delta_2 \right] \\ -z'(h)C\phi_y S\phi_z \Delta_2 - z'(h)S\phi(v) \left[ S\phi_y S\phi_z \Delta_1 - C\phi_z \Delta_2 \right] \\ +x'(h) \left[ S\phi_y S\phi_z \Delta_2 - C\phi_z \Delta_1 \right] \\ z'(h)C\phi_y - z'(h)S\phi(v) \left[ C\phi_z S\phi_z + x'(h)C\phi_z C\phi_x \right] \\ 0 \end{bmatrix}
\]

(16)

Based on the simultaneous solution for the rotational surface matrix of grinding wheel (Eq. (15)) and the structural contour surface equations of tools (Eqs. (5), (6)) in the workpiece coordinates, the grinding wheel position equation is derived during grinding the rake face of the CAMC, as shown in the following:

\[
R_1S \left( \frac{u}{R_1} \right) CR \left( \frac{u}{R_1} \right) = k_3C\phi_y C\phi + k_4 \left[ S\phi_y S\phi_z C\phi - C\phi_z S\phi \right] + k_5 \left[ S\phi_y S\phi_z C\phi + S\phi_z S\phi \right] + a_x C\phi - a_y S\phi
\]

(17)

\[
R_1S \left( \frac{u}{R_1} \right) S \left( \frac{u}{R_1} \right) = k_3C\phi_y S\phi + k_4 \left[ S\phi_y S\phi_z S\phi + C\phi_z C\phi \right] + k_5 \left[ S\phi_y S\phi_z S\phi - S\phi_z C\phi \right] + a_x S\phi + a_y C\phi
\]

(18)

\[
C + R_1C \left( \frac{u}{R_1} \right) = -k_3C\phi_y + k_4C\phi_y S\phi_z + k_5C\phi_y C\phi_x + a_z
\]

(19)

The normal vector of the rotational surface of grinding wheel \( \mathbf{n}_{og} \), the equation for the rotational contour surface of the tool generatrix, and the grinding wheel position equations (Eqs. (17), (18), (19)) are simultaneously solved, and thus the expressions for the normal vector of the rotational surface of grinding wheel is derived during grinding the rake face of the CAMC as follows:

\[
n_1(u) = \frac{-z'(h)C\phi_y S\phi_z - z'(h)S\phi(v) \left[ S\phi_y S\phi_z C\phi - C\phi_z S\phi \right] + x'(h) \left[ S\phi_y S\phi_z C\phi + S\phi_z S\phi \right]}{\sqrt{x'(h)^2 + z'(h)^2}}
\]

(20)

\[
n_2(u) = \frac{-z'(h)C\phi_y S\phi_z - z'(h)S\phi(v) \left[ S\phi_y S\phi_z C\phi - C\phi_z S\phi \right] + x'(h) \left[ S\phi_y S\phi_z C\phi - S\phi_z C\phi \right]}{\sqrt{x'(h)^2 + z'(h)^2}}
\]

(21)

\[
n_3(u) = \frac{z'(h)C\phi_y - z'(h)S\phi(v) \left[ C\phi_z S\phi_z + x'(h)C\phi_z C\phi_x \right]}{\sqrt{x'(h)^2 + z'(h)^2}}
\]

(22)

In grinding the milling cutter, in order to ensure that the grinding wheel was in contact with the workpiece, the relative radial velocity at the contact point was kept 0. Thus, the equation for the relative velocity at the contact point was obtained by differentiating the time on the position matrix of the rotational surface of the grinding wheel (Eq.(15)), as is shown in the following:
than 0.5°. The cutting parameters are detected as follows.

tolerance less than 0.01 mm and the angular tolerance less

instrument made in ZOLLER company was used for measur-
dimensional and angular accuracy. The Genius 3 tool test
quirements, the manufactured CAMC must be detected in the
Grinding site of the CAMC

Figure 6. Grinding site of the CAMC

The equations for the circumferential and end edge curves
of the CAMC were put into the above equation set and solved,
and thus the mathematical models for the grinding wheel po-
face of the CAMC.

3.2 Manufacture and detection of the CAMC

The CAMC was ground on the SAACKE UWI five-axis
grinding center, and the D64 flat grinding wheel and the
11V9 bowl-shape grinding wheel were used. The tool bar
material is the K88UF carbide tungsten steel, its Rockwell
hardness 91.7 HRA, and the particle size 0.8 μm. The grinding
site of the CAMC is shown in Figure 6.

In order to ensure the cutting performance for the use re-
quirements, the manufactured CAMC must be detected in the
dimensional and angular accuracy. The Genius 3 tool test
instrument made in ZOLLER company was used for measur-
ing the accuracy, meeting the demand for the dimensional
tolerance less than 0.01 mm and the angular tolerance less
than 0.5°. The cutting parameters are detected as follows.
For CAMC, the arc radius of end edge $R_1$ is 6 mm, $d_1$ 4
mm, the arc radius of circumferential edge $R_2$ 118 mm, $d_2$ 5
mm, the arc radius of transitional cutting edge $r$ 0.5 mm, and
the lead parameter $p$ 8 mm, while for BEMC, the arc radius of
end edge is 5 mm and the helical angle of side edge 30°.

Figure 7 shows the site and results of detecting the contour
accuracy of the machined CAMC by the tool test instrument.
The red lines represent the theoretical contour and the blue
ones the grinding tolerance zone in the figure. The test results
of grinding accuracy show that the grinding accuracy of the
circumferential edge contour of the CAMC met the require-
ments and there were minor errors in the upper end cutting
edge and the transitional arc areas within the tolerance zone,
so no impact was exerted on the normal use of the cutter.
Furthermore, the derived equation for grinding the CAMC
in this paper can meet the requirement for the accuracy range
in practical machining, so the equation was proved correct and
can be used for manufacturing cutting tools.

4 Comparative experiments on side milling of TC4

4.1 Experimental design

Aiming to evaluate the cutting performance of the CAMC,
this paper designed comparative experiments on side milling
of TC4 titanium alloy using the BEMC and CAMC, and the
experimental site is shown in Figure 8a. The VDL-1000E
three-axis milling center was selected as the machine tool.
The two types of milling cutters for the experiments differed
only in contour, while they were the same in other geometric
parameters. Namely, the diameters were both 10 mm, the hel-
lical angles 30°, the rake angles 6°, the flank angles 12°, and
the edge number 2. The tool material was cemented carbide
tungsten steel, the coating material AlCrN, and the workpiece
material TC4 titanium alloy with a dimension of 150 mm ×
100 mm × 50 mm. In the cutting parameters, the milling ve-
locity was 70 m/min, the feed per tooth 0.06 mm/z, the milling
depth 0.2 mm, and the milling width 0.3 mm.

The CAMC and BEMC are mostly used for machining
inclined end faces of titanium alloy components, and thus
the workpiece surface to be machined was first made into an
inclined plane at an angle of 80° to the horizontal plane before the experiment.

The CAMC and BEMC are mostly used for machining inclined end faces of titanium alloy components. In order to compare the side milling performance of BEMC and CAMC, the workpiece with 80° inclined surface is used for side milling. The specific milling method is shown in Figure 8b.

The Kistler 9139A three-component piezoelectric dynamometer was used in the experiments to collect milling forces. The milling cutter was removed after milling every 3 m, and then the VHX-1000 ultra-depth three-dimensional microscope and the SU3500 scanning electron microscope were used to observe and detect the tool wear morphology. Afterwards, the workpiece was removed, and then the Taylor Surface CCI white light interferometer was used for observing the surface morphology of the machined workpiece. Several standard CAMC and BEMC were ground and tested three times.

4.2 Analysis of cutting performance of the CAMC

Figure 9 shows the comparison of the unworn CAMC and BEMC in milling forces and chip morphology. It is observed...
from the figure that the tangential force generated by the 
BEMC was obviously more than that by the CAMC, while 
the peak values of radial forces were close to each other. This 
is because the CAMC has a cutting edge with larger curvature 
and this decomposed effectively the milling forces in the tan-
gential and axial directions, naturally reducing the radial force. 
Based on the overall change tendency for the chip morphol-
ogy and milling forces, the tangential and radial forces gener-
ated by the CAMC were more stable than the ones by the 
BEMC, and the chips coming from the former were less serr-
ated. The reason for the above is that larger curvature of the 
CAMC cutting edge causes longer cutting edge involved in 
cutting, and chip thinning makes heat dissipation easier so that 
chips are easier to be removed, and thus milling forces are 
more stable.

Figure 10 shows the comparison of the two milling cutters 
in flank wear micromorphology and machined surface quality. 
At the milling length of 60 m, adhesion occurred on both flank 
faces, while a certain amount of coating peeling and tool tip-
ping happened to the BEMC, causing poor surface quality of 
the machined workpiece. Compared with the BEMC, the 
CAMC showed no obvious tool tipping and realized relatively 
flat machined surface at the milling length of 120 m.

Furthermore, the energy spectrum analysis was conducted of 
both milling cutters. Some elements such as O, W, Co, and Ti 
were found in Zone A of the BEMC, indicating that some 
diffusion wear occurred, while only the elements of Ti, Al, 
etc. from the workpiece were found on the flank face of the 
CAMC, showing that only coating peeling appeared. Here, it 
was found that the workpiece surface machined by the BEMC 
was characterized by a large fluctuation in peak and trough 
and the root mean square deviation of surface contour height 
(arithmetic mean deviation of the surface contour height) $S_a$ was 
larger than that by the CAMC.

5 Conclusion

In this paper, the research was conducted on design, manufac-
ture, and cutting performance of circular-arc milling cutters 
(CAMC) for machining titanium alloy. Based on the cutting 
experiments, a comparative analysis was made of milling 
forces, chip morphology, tool wear, and machined surface 
quality in milling titanium alloy with the CAMC and 
BEMC. The conclusions were drawn as follows:

(1) The research on design of the CAMC was carried out.

The contour equations for the end and circumferential
cutting edges of the CAMC were derived by the differential geometry method, and on this basis, the mathematical model for the equal-lead helical edge line of the CAMC was established and verified by MATLAB.

(2) The conversion matrix between grinding wheel and workpiece coordinates was derived, and the mathematical model for the rake face grinding trajectory of the CAMC was established. Grinding the CAMC and testing its geometric accuracy has realized evaluation for the grinding accuracy of developed cutting tools.

(3) Compared with the BEMC, the CAMC shows greater curvature of cutting edge, making the tangential and radial forces more stable in machining. According to the chip morphology, the chips generated by the CAMC are less serrated than the ones by the BEMC, and the unit chip shows no large deformation so that the chip removal is easier.

(4) By contrast with the BEMC, the CAMC is worn slower, shows no diffusion wear, and keeps better cutting performance. With increase of milling length, the residual height and roughness of the workpiece surface machined by the CAMC are still at a low level, and the surface contour changes slowly in shape and displays no obvious defects.

Availability of data and materials The raw/processed data required to reproduce these findings cannot be shared for the time being. Data will be made available upon request.

Author contribution Chen Tao has organized the project, designed the cutting tools, and wrote the manuscript. Liu Gang has designed the cutting tools and wrote the manuscript. Li Rui has conducted the experiments and collected and analyzed data. Lu Yujiang has manufactured and detected the cutting tools; Wang Guangyue has reviewed the manuscript.

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Declarations

Ethics approval The research does not involve human participants or animals, and the authors warrant that the paper fulfills the ethical standards of the journal.

Consent to participate It is confirmed that all the authors are aware and satisfied of the authorship order and correspondence of the paper.

Consent for publication All the authors are satisfied that the last revised version of the paper is published without any change.

Competing interests The authors declare no competing interests.

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