Metamaterials for Remote Generation of Spatially Controllable Two Dimensional Array of Microplasma

Pramod K. Singh1, Jeffrey Hopwood2 & Sameer Sonkusale1

1Nanolab, Department of Electrical and Computer Engineering, Tufts University, Medford, MA, USA-02155, 2Plasma Engineering Laboratory, Department of Electrical and Computer Engineering, Tufts University, Medford, MA, USA-02155.

Since the initial demonstration of negative refraction and cloaking using metamaterials, there has been enormous interest and progress in making practical devices based on metamaterials such as electrically small antennas, absorbers, modulators, detectors etc that span over a wide range of electromagnetic spectrum covering microwave, terahertz, infrared (IR) and optical wavelengths. We present metamaterial as an active substrate where each unit cell serves as an element for generation of plasma, the fourth state of matter. Sub-wavelength localization of incident electromagnetic wave energy, one of the most interesting properties of metamaterials is employed here for generating high electric field to ignite and sustain microscale plasmas. Frequency selective nature of the metamaterial unit cells make it possible to generate spatially localized microplasma in a large array using multiple resonators. A dual resonator topology is shown for the demonstration. Since microwave energy couples to the metamaterial through free space, the proposed approach is naturally wireless. Such spatially controllable microplasma arrays provide a fundamentally new material system for future investigations in novel applications, e.g. nonlinear metamaterials.

Electromagnetic metamaterials are artificial composites made of sub-wavelength metallic structures in a host dielectric medium, engineered to achieve unusual properties not found in the nature. Initial efforts on metamaterial research were focused on the demonstration of negative refractive index1–5 and building a perfect lens2 or cloaking26–27 device. However recently, metamaterials are also being widely studied for various practical applications such as perfect electromagnetic wave absorbers across the broad electromagnetic spectrum from microwave to optical wavelengths8–11, modulators at terahertz frequencies12–13, detectors and imagers14–16, smart antennas and beam shaping devices17–18. Recently, O. Sakai et al. have employed metamaterial to realize negative permeability in the plasma medium to enhance microwave propagation and generation of high density plasma19,20.

In this paper, we utilize metamaterials not as a medium but as a device, where it serves as an active substrate for the generation of plasma within each unit cell of the metamaterial. Metamaterials are typically employed to shape the electromagnetic fields as in the case with many of their prior applications. However in this paper, we exploit one of the most interesting properties of metamaterials that of subwavelength localization of incident electromagnetic energy within the capacitive gap of each metamaterial unit cell at its resonance frequency as the source of energy to ignite and sustain microplasmas. This energy concentration can create sufficiently high electric field to ignite and sustain spatially confined non-thermal microplasmas within each unit cell of the metamaterial array structure. This energy localization at each unit cell of the metamaterial had been utilized in the past for realization of detectors and imagers.

Microplasma is loosely defined as plasma discharges with at least one characteristic dimension smaller than 1 mm and the goal is to be able to generate dense, stable plasmas at atmospheric or near-atmospheric pressures. The plasma medium consists of electrons, ions, molecules which interact strongly in the presence of electric and magnetic fields. For example, the excited electrons in the plasma medium emit light when they relax to the lower energy level and this light emission is an indication of presence of the plasma medium. Microplasma has been studied and used for a wide range of applications such as for material processing21,22, plasma displays23,24, medical treatment24–26, ozone generation27 for water treatment28 and pollution control29,30. Recently, microplasmas have also been suggested for a new class of electronic transistors and devices31–33. Arrays of such microplasmas have significant benefits since they allow creation of plasmas over a large area for these applications. Currently, such
arrays have been demonstrated using dielectric barrier discharges (DBD), DC cavity microdischarges and microwave-frequency resonators. Among them, plasma generation using microwave-frequency resonators is highly promising since it allows plasma generation at low voltages in a wide range of environments including air at atmospheric and near-atmospheric pressures. Microwave discharges provide long operational lifetime since the electrodes are not subjected to unwanted sputtering associated with other methods of plasma generation; this feature is attributed to the relative immobility of heavy ions in microwave fields. Stable arrays in both one and two dimensions have been demonstrated using a single input port for power and utilizing the inherent energy coupling between resonators - as governed by the principles of coupled mode theory - to share this power among the microplasmas in the array. Spatial control of microplasmas in the one dimensional array has also been demonstrated through the embedding of solid state pin diodes for on/off control of individual resonators.

Metamaterials provide a simple realization of a large scale two dimensional array of microplasmas. In metamaterials, subwavelength resonators serve as meta-atoms of an artificial material with unique electromagnetic properties. In its most simplistic realization where the metamaterial is implemented as a single layer as a metasurface, the device is essentially a two dimensional array of resonators as shown in Fig. 1. When designed as an absorber at resonance, a metamaterial will absorb all the incident electromagnetic energy efficiently without reflection. At resonance, the energy is concentrated in the subwavelength capacitive gap of each of the metamaterial unit cells. We explore this subwavelength localization of high microwave energy density to trigger and sustain microwave-frequency microplasmas. Since the incident electromagnetic energy couples through free space, an added significance of the work is wireless operation for the generation of an array of microplasmas on metamaterial substrate. An overall sketch for the free space excitation and remote generation of microplasmas in metamaterial is shown in Fig. 1. The detailed experimental setup is shown in the supplementary section (Fig. S4).

Results
As shown in Fig. 1 the microwave energy is provided wirelessly from a patch antenna radiating in free space towards the metamaterial surface (or metasurface) which consists of a periodic distribution of unit cells made of ‘C’ shaped split ring resonators (SRR). Microwave energy coupled to the metamaterial generates a high electric field in the micrometer sized (150 microns) split gap of the SRR at the resonance frequency. When this electric field is high enough the argon gas atoms are ionized to form plasma in and around the gap region. Since metamaterials are inherently frequency selective, i.e. the energy coupling to it is maximum only at the resonance frequency of the individual resonators (or meta-atoms), one can engineer the metasurface to have more than one resonance frequency by using multiple resonators (or meta-atoms) in its realization where different meta-atoms are resonant at different frequencies. Moreover, one can also geometrically arrange these meta-atoms in a certain spatial pattern on this meta-surface for additional control over the geometrical pattern of microplasmas. To verify the frequency selectivity, a dual frequency metamaterial is designed which contains two resonators that have distinct resonance frequencies (2.1 GHz and 2.45 GHz). When this metamaterial is irradiated by microwave energy, the plasma is generated in only the one set of resonators that has the same frequency as the incident microwave radiation. And when irradiated with microwave energy with a frequency of the second set of resonators, then the microplasmas are generated in the other set of resonators. Thus, one can spatially control the generation of microplasmas by choosing an appropriate frequency of incident radiation and placement of resonators in metamaterial array.

The photograph of the dual frequency metamaterial board is shown in Fig. 2 (a). Two resonators which are different in size result in two separate resonance frequencies. The larger size resonator has a lower resonance frequency (2.1 GHz). These two resonators are periodically distributed in a 2-dimensional array (any other pattern could also be chosen). The board consists of a 6 × 6 array of 36 resonators, 18 each for the two different resonance frequencies. For each C-shaped resonator, the width of metal line is tapered down to 0.7 mm from the original width of 1 mm near the capacitive gap to increase the energy concentration for microplasma generation. Two patch antennas are used to radiate microwave energy at two different resonant frequencies of the metamaterial that are used interchangeably. Simulation and measurement of the power transmission through the dual frequency metamaterial surface is shown in Fig. 2(b). It clearly shows two resonances, one at 2.1 GHz and another at 2.45 GHz. Small shifts in measured resonant frequency (0.01 GHz) are observed compared to simulation results due to process variations in the actual fabrication of the device. Electric field distribution is simulated at these two resonance frequencies, i.e. the energy coupling to it is maximum only at the resonance frequency of the individual resonators (or meta-atoms), one can geometrically arrange these meta-atoms in a certain spatial pattern on this meta-surface for additional control over the geometrical pattern of microplasmas. To verify the frequency selectivity, a dual frequency metamaterial is designed which contains two resonators that have distinct resonance frequencies (2.1 GHz and 2.45 GHz). When this metamaterial is irradiated by microwave energy, the plasma is generated in only the one set of resonators that has the same frequency as the incident microwave radiation. And when irradiated with microwave energy with a frequency of the second set of resonators, then the microplasmas are generated in the other set of resonators. Thus, one can spatially control the generation of microplasmas by choosing an appropriate frequency of incident radiation and placement of resonators in metamaterial array.

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To radiate microwave power, two patch antennas are designed to wirelessly feed power to the metamaterial at two different resonance frequencies, 2.1 GHz and 2.45 GHz. Layout of the patch antenna is selected to provide wider bandwidth for wireless radiation.
Microwave output power from the power amplifier was increased in steps from 2 W to 50 W. Plasma was ignited (in argon gas at pressure of 40 Torr) at the power level of 30 W in the set of resonators of the same frequency as that of the incoming microwave radiation. The power level was further increased up to 50 W and at this power level plasma starts in the patch antenna itself (at the SMA connector position). This essentially limits the maximum power level of patch antenna that can be transmitted. Power level of 40 W was set to generate the plasma for the photographs reported in this paper.

The experiment is repeated with microwave radiation once at 2.1 GHz and another at 2.45 GHz to correspond to the two different resonance frequencies of the metamaterial. Figure 3 shows that microplasma is generated in one set of resonators when excited at 2.1 GHz (Fig. 3a) and in another set of resonators when excited at 2.45 GHz (Fig. 3b). In both cases, there was one resonator that did not produce any plasma. This is attributed to the increase in the gap size of the resonators (0.203 mm and 0.198 mm instead of the expected 0.15 mm) due to fabrication error which resulted in reduced electric field intensity not sufficient for the generation of plasma in these resonators. Total radiated power from the antenna can at maximum be 0.78 W (14 W/18) at 2.1 GHz and 1.28 W at 2.45 GHz. The actual power that causes microplasma ignition will be lower since some power radiated from the antenna is not directly incident and is either reflected or scattered by the metamaterial board. Exact determination of the power levels was not currently possible in our experimental setup.

Figure 2 | (a) Photograph of a dual frequency metamaterial board, (b) measured and simulated microwave power transmission results for the metamaterials showing two resonance frequency at 2.1 GHz and 2.45 GHz respectively, the inset shows simulated electric field at resonance frequencies in the metamaterial structure – only the resonator with resonance at frequency of incident radiation shows maximum electric field (c) photograph of the patch antenna at 2.1 GHz used for microwave radiation, and (d) simulated and measurement results of the 2.1 GHz patch antenna, inset shows simulated antenna power radiation pattern.

Figure 3 | Wireless plasma generation in dual frequency metamaterials in argon gas at pressure of 40 Torr. Plasma is generated in only array of resonators working at (a) 2.1 GHz and (b) 2.45 GHz.
For the generation of a larger array of microplasmas, a metamaterial board consisting $10 \times 10$ unit cells with a single resonance frequency of 2.45 GHz is designed (supplementary section Fig. S5). Also, one important parameter of interest for plasma generation, especially for electronic applications, is the carrier concentration in plasma; and it increases with the increase in the gas pressure. Generating plasma at atmospheric pressure (760 Torr) is therefore useful in order to increase the carrier concentration. Plasma generation at atmospheric pressure was investigated in a single frequency metamaterial board consisting 100 unit cells. Paschen’s Law describes that higher microwave power is required to initiate plasma at higher gas pressure. A pulsed microwave source with peak power of 500 W (available in conventional commercial microwave oven) is used to generate the plasma at atmospheric pressure at a single frequency of 2.45 GHz. The photograph of the metamaterial with plasma at atmospheric pressure in argon is shown in Fig. 4. Plasma is generated in 90 resonators out of 100 elements (90% yield); fabrication error was responsible for the unit cells that did not ignite. Measurement of carrier density was not possible with the current setup. Morjiev et al. has reported an electron density of $3 \times 10^{12}$ cm$^{-3}$ in microwave argon plasma at atmospheric pressure which was an order of magnitude higher than the plasma at 50 Torr$^{42}$. Recently, in our prior work, Hopwood et al. measured electron density of $3 \times 10^{13}$ cm$^{-3}$ in atmospheric pressure argon microwave plasma$^{43}$.

While one can utilize an array of microplasmas for a variety of applications, we exploit the high nonlinearity of plasmas to realize a non-linear metamaterial. Nonlinear metasurfaces are an emerging class of artificial materials with exciting applications in frequency generation$^{44-46}$ and parametric amplification$^{47,48}$; they are realized today using varactor loaded split ring resonators which are difficult to scale up due to electrical routing requirements. The electromagnetic properties of the metamaterial medium can be altered by changing the capacitance of the varactor in the gap of each unit cell$^{49}$ and in our case by the nonlinearity of the microplasma in the gap of each split ring resonators. These change of nonlinearity with incident field can be exploited for harmonic generation$^{46}$.

Of these applications, we show preliminary results of higher order harmonic generation; single sources of plasma have been utilized in the past for harmonics generation$^{46}$. To observe this nonlinear effect, the emitted spectrum from the metamaterial is recorded where harmonics of the excitation sources can be seen. The measurements show power levels of fundamental frequency (2.45 GHz, $-13$ dBm), second harmonic (4.9 GHz, $-51$ dBm), third harmonic (7.35 GHz, $-49$ dBm) and fourth harmonic (9.8 GHz, $-57$ dBm) (see supplementary section Fig. S6). The results, while not optimized for this application, clearly indicate that metamaterials can be used as an array to generate high frequency power using higher order harmonic generation. Other applications such as a gain medium using parametric amplification can also be envisioned$^{46,48}$.

Discussion

Metamaterials enable a unique application working as a substrate for the remote generation of spatially defined arrays of microplasmas. Frequency selective spatial localization of microplasmas in a large array can be realized using multiple resonators. Results for a metamaterial with a dual resonator configuration showed that microplasmas are generated spatially in only selected resonators whose resonance frequency is matched to that of incident radiation. Since microwave energy can be fed wirelessly to the metamaterials, the results demonstrate a remote generation of arrays of spatially localized subwavelength microplasmas without the use of any wires. Moreover the electron density in the argon plasma at atmospheric pressure can be much higher than at lower pressure, providing a unique electronic material system with possibly novel functions. Since microplasma could be generated over a large area with a spatially defined pattern, it could be used for many applications such as in the realization of a high-frequency source, where one could exploit the nonlinearity of the plasma for higher order harmonic generation and parametric amplification. This is especially promising in making devices for the terahertz gap in the electromagnetic spectrum.

Methods

Metamaterial and patch antennas are designed using electromagnetic simulation software (CST Microwave Studio®). The metamaterial board is fabricated on a dielectric substrate (Rogers RO4003C, 0.8 mm thickness) by machining 17 micron thick copper metal (using LPKF Protomat CNC machine) to form the resonators (metamaterial unit cells). S-parameters are measured using a vector network analyzer setup. For the plasma generation experiment, devices were placed in a chamber which was then evacuated to a base pressure of $4 \times 10^{-5}$ Torr and again filled with argon gas up to a required pressure. Metamaterial board and antenna were placed in holders facing each other as shown in the schematic in Fig. 1 (see supplementary Fig. S4). Microwave power was fed to the antenna from a solid state power amplifier. Images of plasma were collected by looking through a UV protected transparent glass window and through an additional metal mesh in the case when high microwave power was applied.

Figure 4 | Metamaterial board of $10 \times 10$ elements generating plasma at atmospheric pressure and microwave frequency of 2.45 GHz. Plasma is generated in 90 elements out of 100 elements. Photograph is taken through a metal mesh.

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