Physical Reasoning in an Open World

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Abstract

Most work on physical reasoning, both in artificial intelligence and in cognitive science, has focused on closed-world reasoning, in which it is assumed that the problem specification specifies all relevant objects and substance, all their relations in an initial situation, and all exogenous events. However, in many situations, it is important to do open-world reasoning; that is, making valid conclusions from very incomplete information. We have implemented in Prolog an open-world reasoner for a toy microworld of containers that can be loaded, unloaded, sealed, unsealed, carried, and dumped.

1. Introduction: Open vs. closed world reasoning

Consider the following scenarios:

A.1 You pack clothes and a tube of toothpaste in a duffel bag, you lock the zipper, you check it onto a flight to Chicago. The duffel bag is lost. Three days later, it turns up at the Dallas airport. It's pretty scuffed up, but intact. Who knows what they did to it or how it got there. However, if it’s still locked, you can be sure that the clothes are still inside, but it will not be very surprising to find that there is now toothpaste over everything in the bag.

A.2 In an archaeological site, a male human skeleton is found with a broken ulna that healed. You can infer that during his lifetime, the person broke his arm and then it healed, though you know essentially nothing else about the person’s life or what has happened to the skeleton between the time he died and the time it was found.

A.3 A hurricane is predicted for where you live, so you take appropriate actions: you board up the windows, bring in the lawn furniture, stock up on water and so on. These are all sensible precautions, even though you cannot predict exactly what will happen; e.g. which, if any, of your windows would break if you did not board them up.

A.4 A condominium suddenly collapses. You fear that anyone who was inside and did not manage to escape is gravely injured or dead. Note that you can make this inference even if you have never before heard of a condominium spontaneously collapsing and would not have supposed that it was possible.
From the standpoint of reasoning, what these have in common is that they all deal with open-world scenarios, in which one must carry out reasoning with very limited knowledge of the events that occurred and the objects that are involved.

As the above examples illustrate, open-world physical reasoning is common and important in real life situations. However, it has rarely been studied in AI literature and is almost completely unstudied in cognitive psychology. Instead, the focus of earlier research in physical reasoning has been almost entirely on closed-world reasoning, in which it is assumed that all the physical entities that are relevant are enumerated, all aspects (to some fixed level of detail) of an initial state are stated, and that all the relevant events are either enumerated or can be inferred from a dynamic theory.

We have developed a proof-of-concept logic-based reasoner, implemented in Prolog, for doing open-world reasoning about a toy world in which an agent can manipulate containers. In our microworld, objects can be loaded into containers or unloaded from them; objects can be carried from one location to another; an open container can be closed with a lid, and a lidded container can be opened. Our system doesn’t deal with shapes and sizes; any object or set of objects can be put inside any open container.

Our program can handle examples such as the following:

B.1 Over the interval \([T_1, T_2]\) object \(OB\) is put into open container \(OC\). Over the interval \([T_2, T_3]\) container \(OC\) is closed with lid \(OL\). Between \(T_3\) and \(T_4\), the lid is not opened. Infer that \(OB\) is still inside \(OC\) at time \(T_4\).

B.2 Over the interval \([T_1, T_2]\) object \(OB\) is put into open container \(OC\). Suppose between \(T_2\) and \(T_3\), \(OB\) is not unloaded from \(OC\) and no object is overturned (“dumped”). Then we can safely infer that at \(T_3\), \(OB\) will still remain in \(OC\).

B.3 Over the interval \([T_1, T_2]\) object \(OB\) is put into open container \(OC\). Suppose between \(T_2\) and \(T_3\), \(OC\) is carried from location \(A\) to location \(B\). This will not change the fact that, at \(T_3\), \(OB\) is still contained in \(OC\) and has been carried together with \(OC\) to location \(B\).

Equally important are the inferences that cannot be made in an open world. For instance suppose that you are given that at time \(T_1\), object \(OB\) is inside open container \(OC\), and that time \(T_2 > T_1\). In a closed world, one can infer that \(OB\) remains inside \(OC\) at time \(T_2\), since there is no reason to suppose that it has come out. In an open world, this inference cannot be made, since \(OB\) may have been removed from \(OC\) in between.

The microworld and the examples are certainly very limited, but the analysis reveals aspects of dealing with open-world physical reasoning that are likely to be important in broader settings.

Section 2 will review related work. Section 3 will discuss the microworld that our system works in. Section 4 will discuss reasoning in the abstract. Section 5 will discuss the implementation. Section 6 will discuss future work.
2. Related Work

2.1 Open-world physical reasoning

Physical reasoning tasks generally involve the following elements:

- A number of objects or substances (broadly speaking). These have properties and relations, some numeric, some non-numeric, some fixed over time, some time-dependent.
- A starting situation: the state of the world at $t = 0$.
- A system trajectory: What happens over a time interval.
- (Optional) Some number of exogenous events or actions: Events that take place due to external influences such as agents, that cannot be predicted from the theory.
- A dynamic theory: The physical laws that govern the spontaneous evolution of the system and its response to exogenous events.

The distinction between closed and open world physical reasoning is not a binary dichotomy. Rather, the information available in different classes of reasoning problems can vary along a number of dimensions.

- The numerical and geometric information about the starting situation may be exact, approximate, probabilistic, qualitative, or partial. (These are not mutually exclusive.)
- The other properties and relations that hold in the initial situation may be completely specified or partially unspecified.
- The objects that enter into the trajectory may be enumerated.
- Exogenous events may be completely specified or partially specified.
- The dynamic theory that governs the phenomena may be exact, approximate, probabilistic, qualitative, or partial.

The “most closed” form of closed world physical reasoning is deterministic prediction: the starting situation is completely specified in all aspects (up to some level of precision); exogenous events or boundary conditions are likewise completely specified; the dynamic theory is complete and exact. The reasoning task is, given the initial situation, exogenous events, and dynamical theory, to predict the exact trajectory (again, up to some level of precision). “Physics engines”, such as those that power video games, are almost all in this category, as is the majority of scientific simulation.

In probabilistic (Monte Carlo) simulation, probability distributions are specified for the initial situation and the dynamic theory is probabilistic; the task is to generate samples from the corresponding probability distribution over the trajectories. In cognitive psychology, this is often called the “noisy Newton” approach (Gerstenberg et al., 2012). In a fully observable scenario, the reasoner is given a complete description of the current state; in a partially observable scenario, they are given
Knowledge-based AI physical reasoning:

**Deterministic prediction:** (Funt, 1980), (Zickler & Veloso, 1999).

**Probabilistic prediction (Monte Carlo):** Rare.

**Partially observable states:** Rare.

**Qualitative envisionment:** (Forbus, 1985), (de Kleer and Brown, 1985).

**Inverse reasoning:** Rare.

**Radically incomplete reasoning:** (Hayes, 1979) (Davis, Marcus, and Frazier-Logue 2017).

Cognitive psychology:

**Deterministic prediction:** (Schwartz & Black, 1996), (Smith, Battaglia, & Vul, 2018).

**Probabilistic prediction (Monte Carlo):** (Battaglia, Hamrick, & Tenenbaum, 2013),
(Gerstenberg, Goodman, Lagnado, & Tenenbaum, 2012).

**Partially observable states:** (Sanborn, 2014).

**Qualitative envisionment:** (Forbus & Gentner, 1997).

**Inverse reasoning:** (Sanborn, Mansinghka, & Griffiths, 2013).
(Bramley, Gerstenberg, Tenenbaum, & Gureckis, 2018)

**Radically incomplete reasoning:** Rare.

Scientific computing

**Deterministic prediction:** (Dahlquist & Björck, 2008).

**Probabilistic prediction (Monte Carlo):** (Liu, 2001)

**Partially observable states:** ?? We don’t know.

**Qualitative envisionment:** None.

**Inverse reasoning:** (Vogel, 2002)

**Radically incomplete reasoning:** None.

*Table 1.* Some examples of different kinds of physical reasoning

Only partial or probabilistic information. In qualitative reasoning, the initial situation and dynamic theory are given in qualitative terms; the task, typically, is to compute the possible trajectories in qualitative terms. In inverse problems, the trajectory is given and the task is to infer the values of various numerical or geometric parameters. One can further usefully distinguish between inverse problems in which the given information determines all aspects of the scenario and those where it does not. In theory induction a collection of trajectories are given, and the task is to infer the underlying dynamical theory, or the most likely one, within some space of possible candidates under consideration.

There is also large body of work on AI planning in partially observable worlds such as POMDPS in which the starting state and subsequent states are only partially characterized including high-level planning (e.g. Eiter et al. 2000), robotic planning (e.g. Hahnheide et al. 2017), and adversary games (e.g. Bethe, 2020; Brown and Sandholm, 2019). There is a small body of work of this kind in the cognitive psychology literature on physical reasoning; e.g. problems involving reasoning about collisions between objects of unknown mass (Sanborn, 2014). However, there is little work in this...
category in AI physical reasoning. How much work on scientific computation with partially observable states, we do not know.

The “most open” form of physical reasoning is reasoning that is *radically incomplete* (Davis, Marcus, & Frazier-Logue, 2017). That is, the information given is so weak that the full trajectory cannot be inferred; only some facts can be inferred. For example, in example A.1, you cannot know how exactly the duffel bag got to Dallas or who did what to it *en route*. In example B.1, you cannot know where $OC$, $OL$, and $OB$ are located at time $T_4$, since the lidded container may have been moved to some other location between times $T_3$ and $T_4$. Analyses based on monotonic logics are often appropriate to open-world reasoning — in monotonic logics, closed world assumptions must be asserted explicitly — but, previously, these have hardly been implemented. (Situation calculus was designed primarily for closed-world planning; hence, general open world physical reasoning tends to be awkward, even in monotonic formulations.)

Table 1 gives some typical references for examples of the various types of inference in the AI physical reasoning literature, cognitive psychology, and scientific computing. The literature in many of these categories is large; in some, it is enormous.

### 2.2 Reasoning about containers

AI studies of reasoning about containers have mostly been in theoretical studies of logical reasoning, with no implementated reasoner (Hayes, 1979; Hayes, 1985; Davis, 2008; Davis, 2011; Davis, Marcus, & Frazier-Logue, 2017).

In cognitive psychology, reasoning about containers has primarily been studied in small children (Aguiar & Baillargeon, 1998; Hespos & Baillargeon, 2006). It has been demonstrated (Hespos & Baillargeon, 2001) that children as young as 2-1/2 months understand some of the physical properties of containers — for instance, the fact that an object cannot be put into a closed container.

### 3. The Microworld

The microworld includes five sorts of entities: objects, locations, actions, times, and states (Boolean fluents).

There are five kinds of objects:

- **Closed containers.** A closed container has an internal cavity that may contain other objects. It cannot be opened. Objects are either outside or inside forever.

- **Open containers.** An open container has an cavity with an opening on top. Other objects can be loaded into an open container.

- **Lids.** A lid can be used to close an open container.

- **Lidded containers.** This is a pair of an open container and a lid; it functions as a single object. It acts as a temporary closed container; nothing can come in or out until the lid is taken off.

- **Blocks.** None of the above. Blocks can be put into containers but cannot contain anything.
The idea that any kind of container can be used for any kind of content is, of course, a huge idealization. In reality, the question of whether A can serve as a container for B involves complex interactions of spatial and physical properties. A string shopping bag can be used as a container for a potato but not for a pea. A bird cage can be used to contain a canary. It cannot be used to contain an ant, because the ant can crawl out; it cannot be used to contain a gorilla, because the gorilla is too large. A lucite box is a closed container as regards air, but light passes freely in an out. The spatial and physical reasoning involved in the cases where all the objects involved are rigid solid objects is in principle characterized in theories like (Davis, Marcus, & Frazier-Logue, 2017), though it has not been implemented in a reasoner. Reasoning about flexible containers such as string bags is terra incognita. (Physics engines can certainly deal with simple cases of containment with rigid solid objects, though not elegantly. However, once the containment relation becomes complex, they have trouble; for instance, though doors are common in video games, very few game engines use a physically realistic model (Farokhmanesh, 2021).) For the purpose of this initial investigation, we ignore all these issues.

The Prolog predicate \texttt{components(OC, OL, OW)} means that the lidded container \textit{OW} consists in the open container \textit{OC} and lid \textit{OL}. (Throughout this paper, we will use typewriter font for Prolog and for logical formulas. Following a common Prolog convention, variables will start with an upper case character; predicates, functions, and constants will start with a lower case character.)

An object is \textit{top-level} at a given time if it is not inside any other object and not a component of a lidded container.

Locations in this theory are general areas; any number of objects may be at a particular location. Locations have no properties, except the objects that are at them.

There are six kinds of actions:

- Carrying object \textit{O} to location \textit{L}; in our Prolog notation, \texttt{carry(O, L)}. Any top-level object can be carried to any location. Any objects contained inside \textit{OA} remains inside \textit{OA}.

- Loading object \textit{O} into open container \textit{OC}: \texttt{load(O, OC)}. \textit{O} and \textit{OC} must both be top-level and at the same location. If \textit{O} itself is a container and \textit{OB} is contained in \textit{O}, then \textit{OB} remains in \textit{O}. (Containers are loaded carefully, so that their contents do not spill).

- Unloading object \textit{O} from open container \textit{OC}: \texttt{unload(O, OC)}. \textit{OC} must be top-level and \textit{O} must be directly contained in \textit{OC}. The result of unloading is that \textit{O} is now top-level at the same location as \textit{OC}. If \textit{O} itself is a container and \textit{OB} is contained in \textit{O}, then \textit{OB} remains in \textit{O}.

- Sealing open container \textit{OC} with lid \textit{OL} forming lidded container \textit{OW}: \texttt{seal(OC, OL, OW)}. \textit{OL} must fit on \textit{OC}, and both must be top-level at the same location. As a result, the composite container \textit{OW} becomes “effective” and \textit{OC} and \textit{OL} become “ineffective”.

- Unsealing lidded container \textit{OW} and splitting it into open container \textit{OC} and lid \textit{OL}: \texttt{unseal(OW, OL, OC)}. \textit{OW} must be top-level and effective. \textit{OW} becomes ineffective and \textit{OC} and \textit{OL} become effective.
• Dumping a container: \( \text{dump}(O) \). Intuitively, turning it upside down, and letting the contents spill out. If container \( O \) get dumped, then, recursively, all the containers inside \( O \) get dumped. If container \( OA \) gets dumped, and object \( OB \) is contained in \( OA \), directly or indirectly, then \( OB \) gets dumped. If \( OB \) is inside \( OC \) (possibly equal to \( OA \)) which is a closed container or an lidded container, then \( OB \) remains inside \( OC \). If \( OB \) is not inside any closed container, then it falls to the ground outside. Figure 1 shows an example.

Five kinds of states (Boolean fluents) are used to characterize these actions:

• \( \text{outsideAt}(O, L) \): Object \( O \) is at location \( L \), not inside any container.

• \( \text{directContained}(OA, OC) \): Object \( OA \) is directly contained in object \( OC \).

• \( \text{contained}(OA, OB) \). Object \( OA \) is directly or indirectly contained in \( OB \). The non-reflexive transitive closure of \( \text{directContained}(OA, OB) \).

• \( \text{effective}(O) \): Object \( O \) exists and can be individually manipulated.

• \( \text{ineffective}(O) \): Object \( O \) either does not exist (a potential lidded container that has not been assembled) or cannot be separately manipulated (an open container or a lid that is part of an assembled lidded container).

Named instants of time are linearly ordered by the relation \( \text{earlier}(T_1, T_2) \). This relation means that, among the instants named in the problem specification, \( T_1 \) immediately precedes \( T_2 \); it does not mean that they are sequential in the actual time line. In particular, any number of unnamed events may have occurred between \( T_1 \) and \( T_2 \). Indeed, the theory of time is agnostic as to the kind
of linear ordering of the actual time line; the time line may correspond to integers, to real numbers, or are some other kind of linear ordering. Thus, the theory could easily be extended to reasoning in a dense or continuous model of the time line. We do make the assumption that there are never two events occurring simultaneously, since the causal theory of simultaneous events tends to be much more complicated.

Following (McDermott, 1982), we use the predicate holds($T, S$) to mean that state $S$ holds at time $T$, and the predicate occurs($T_1, T_2, E$) to mean that event/action $E$ occurs between time points $T_1$ and $T_2$.

4. Open world reasoning and the frame inference

The key feature of the kind of open world reasoning that we are studying in this project is the ability to do partial prediction over intervals in which it is not known what events occurred. Of course, if there is no information at all about what happened between time $T_A$ and time $T_B$, then the only states that can be excluded in $T_B$ are those that are entirely unreachable from the situation in $T_A$ by any sequence of events. In our microworld, the only simple states of this kind are the contents of a closed container, which cannot be changed. (There are also, additionally, unattainable conjunctions; it is impossible that $OA$ is contained in $OB$ and $OB$ is contained in $OA$; it is impossible that object $O$ is both at location $LA$ and location $LB$.)

In general, to infer that a given state $S$ that holds in $T_A$ will continue to hold in $T_B > T_A$, it suffices to know that none of the events that would cancel $S$ occur between $T_A$ and $T_B$. This can be carried out in a logic-based system using frame axioms stated as explanation closure axioms (Schubert, 1994) which specify necessary conditions for a fluent to change values. For example, in our microworld, there is an axiom stating that if object $OA$ is contained in a closed container with lid $OW$ at time $T_1$ and is not contained in $OW$ at time $T_2$, then, at some time in between $T_1$ and $T_2$, $OW$ must have been opened.

Let us first define the predicate occursWithin($T_A, T_B, E$) to mean that there is an occurrence of $E$ that overlaps the interval $[T_A, T_B]$.

$$\forall_{T_A,T_B,E} \text{ occursWithin}(T_A, T_B, E) \iff \text{earlier}(T_A, T_B) \land \exists_{T_C,T_D} \text{ earlier}(T_C, T_D) \land \text{ earlier}(T_C, T_B) \land \text{ earlier}(T_A, T_D) \land \text{ occurs}(T_C, T_D, E).$$

We can now formally state the above frame axiom:

Frame axiom F.1:

$$\forall_{OA, OC, OL, OW, T_1, T_2} \text{ earlier}(T_1, T_2) \land \text{ containerWithLid}(OW) \land \text{ components}(OC, OL, OW) \land \text{ holds}(T_1, \text{ effective}(OW)) \land \text{ holds}(T_1, \text{ contained}(OA, OW)) \land \neg \text{ holds}(T_2, \text{ contained}(OA, OW)) \Rightarrow \text{ occursWithin}(T_1, T_2, \text{ unseal}(OC, OL, OW)).$$
The contrapositive of F.1 is the frame inference: If \( OA \) is contained in sealed container \( OW \) at \( T1 \) and no unsealing of \( OW \) occurs within \([T1, T2]\) then \( OA \) is still contained in \( OW \) at \( T2 \).

\[ \forall_{OA,OC,OL,OW,T1,T2} \text{earlier}(T1,T2) \land \text{containerWithLid}(OW) \land \text{components}(OC,OL,OW) \land \text{holds}(T1,\text{effective}(OW)) \land \text{holds}(T1,\text{contained}(OA,OW)) \land \neg \text{occursWithin}(T1,T2,\text{unseal}(OW,OL,OC)) \Rightarrow \text{holds}(T2,\text{contained}(OA,OB)). \]

5. Implementation

We have implemented an inference engine for open-world reasoning for this microworld in Prolog.\(^1\) A problem specification consists in

- A sequence of time instance, completely ordered under the \text{earlier} relation.
- A collection of statements of the form \( \text{holds}(T,Q) \). Often these are all stated at some starting time \( t0 \), but specifications can include assertions about other times as well.
- A collection of statements of the form \( \text{occurs}(TA,TB,E) \). The intervals for different actions may not overlap temporally.
- A collection of statements that specific action do not occur within particular intervals. As we will discuss in section 5.2 because of idiosyncracies of Prolog, these take a number of different forms.

There are two key predicates characterizing change. The first is \( \text{condEffect}(E,\text{GOAL},\text{QLIST}) \), which means that, if \( E \) occurs from \( T1 \) to \( T2 \) and all the states in \( \text{QLIST} \) hold in \( T1 \) then \( \text{GOAL} \) will hold in \( T2 \). For example, in implementing example B.1, we use the following:

\[
\begin{align*}
% If you load OB into OC, then OB is (unconditionally) inside OC. 
\text{condEffect}(\text{load}(OB,OC),\text{contained}(OB,OC),[]).
\end{align*}
\]

\[
\begin{align*}
% If OA is contained in OB at time T1 and you load OB into OC 
% from T1 to T2, then OA will be contained in OC at T2. 
\text{condEffect}(\text{load}(OB,OC),\text{contained}(OA,OC),[\text{contained}(OA,OB)]).
\end{align*}
\]

\[
\begin{align*}
% If OA is directly contained in OC at time T1 and you seal OC 
% with lid OL forming OW from T1 to T2, then OA is directly 
% contained in OW at T2 
\text{condEffect}(\text{seal}(OC,OL,OW),\text{contained}(OA,OW),[\text{contained}(OA,OC)]).
\end{align*}
\]

\(^1\)https://github.com/Jennifercheukyin/Physical-Reasoning-in-Open-World
Note that the conditions are not the preconditions of action $E$, which must be true for the action to be executed. In fact, our implementation of infer does not deal with action preconditions at all. The occurrence of the action is given as a boundary constraint (presumably it is observed or stated), so necessarily the preconditions are satisfied.

The second key predicate is $\text{persistence}(TA, TB, Q)$. This means that, if $Q$ is true at time $TA$ then it will still be true at time $TB$. This holds if either (a) the problem specification asserts that $\text{occurs}(TA, TB, E)$ and $E$ does not change $Q$; or (b) if the problem specification asserts that none of the actions that change $Q$ occur within $[TA, TB]$.

For instance, for the example below, we will use the rule, “If the lidded container $OW$ is not unsealed in any interval overlapping $T1$ and $T2$, then the condition ‘$OA$ is contained in $OW$’ persists from $T1$ to $T2$.”

$$\text{persistence}(T1, T2, \text{contained}(OA, OW)) :-$$
$$\text{containerWithLid}(OW),$$
$$\text{components}(OC, OL, OW),$$
$$\text{infer}(\text{holds}(T1, \text{effective}(OW))),$$
$$\text{notOccurs}(T1, T2, \text{unseal}(OW, OL, OC)).$$

(We use the Prolog predicate $\text{notOccurs}(T1, T2, E)$ to mean the logical formula $\neg \text{occursWithin}(T1, T2, E)$. The need for this is discussed in section 5.2.)

The reasoning engine is the query $\text{?-- infer}(\text{holds}(T, Q))$. It uses recursive backward chaining through time.

State $Q$ holds at time $T$ if either

a. The problem specification asserts $\text{holds}(T, Q)$.
b. The problem specification asserts $\text{occurs}(TX, T, E)$, the world model asserts $\text{condEffect}(E, Q, L)$, and the inference engine can recursively verify $\text{infer}(TX, G)$ for every goal $G$ in $L$.
c. Let $TA$ be the time instant preceding $T$ in the earlier relation. The recursive subgoal $\text{infer}(\text{holds}(TA, Q))$ succeeds and the inference engine can validate $\text{persistence}(TA, T, Q)$.

Thus, in Prolog we have the top-level code

$$\text{infer}(\text{holds}(T, Q)) :- \text{holds}(T, Q). \ % \text{Rule 1}$$

$$\text{infer}(\text{holds}(T, Q)) :-$$
$$\text{occurs}(TA, T, ACT),$$
$$\text{condEffect}(ACT, GOAL, QLIST),$$
$$\forall \text{member}(Q, QLIST), \text{infer}(\text{holds}(TA, Q)). \ % \text{Rule 2}$$

$$\text{infer}(\text{holds}(T, Q)) :-$$
$$\text{earlier}(TA, T), \text{infer}(\text{holds}(TA, Q)), \text{persistence}(TA, T, Q). \ % \text{Rule 3}$$
In view of the complexity of the effects of actions like dumping in this microworld — both recursive and context-dependent — the effects of actions are individually coded, rather than being simple add lists and delete lists.

5.1 Example B.1 in Prolog

Example B.1 discussed above can be encoded with the following specification:

\[
\begin{align*}
\text{block(oa). openContainer(oc). lid(ol). containerWithLid(ow).} \\
\text{components(oc,ol,ow). location(la).} \\
\text{earlier(t0,t1). earlier(t1,t2). earlier(t2,t3).} \\
\text{holds(t0,\text{outsideAt}(oa,la)).} \\
\text{holds(t0,\text{outsideAt}(oc,la)). holds(t0,\text{outsideAt}(ol,la)).} \\
\text{holds(t0,\text{effective}(oc)). holds(t0,\text{effective}(ol)).} \\
\text{holds(t0,\text{ineffective}(ow)).} \\
\text{occurs(t0,t1,\text{load}(oa,oc)).} \\
\text{occurs(t1,t2,\text{seal}(oc,ol,ow)).} \\
\text{notOccurs(t0,t3,\text{unsealToAnything}(ow))} \\
\end{align*}
\]

(The strange form notOccurs(t0,t3,unsealToAnything(ow)) will be explained in section 5.2.)

The query \(\text{?- infer(holds(t3,\text{contained}(oa,ow))}\) succeeds, using the following inference path:

Rule 3 for infer creates the subgoal \(\text{?- infer(holds(t2, \text{contained}(oa,ow)))}\). We now apply Rule 2: Since \(\text{contained}(oa,ow)\) is an effect of \(\text{seal}(oc,ol,ow)\) given the condition \(\text{contained}(oa,oc)\), we create the subgoal \(\text{holds(t1,\text{contained}(oa,oc))}\). Applying Rule 2 again, we find that this holds since \(\text{contained}(oa,oc)\) is an unconditional effect of \(\text{load}(oa,oc)\).

Returning to the first application of Rule 3, we create the subgoal

\(\text{?- persists(t2,t3,\text{contained}(oa,ow))}\).

Using the persistence rule stated earlier, plus additional rules (not stated here) that allow us to infer
\(\text{notOccurs(t2,t3,\text{unseal}(ow,ol,oc))}\) from
\(\text{notOccurs(t0,t3,\text{unsealToAnything}(ow))}\) and the order on time points, we satisfy the persistence subgoal. That completes the inference of the top-level query
\(\text{?- infer(holds(t3,\text{contained}(oa,ow)))}\).

By contrast, the query \(\text{?- infer(holds(t3,\text{outsideAt}(ow,la))}\) fails because it is consistent with our information that \(\text{ow}\) is carried to some other, unnamed, location, between \(t_2\) and \(t_3\).
5.2 Issues with Prolog

We chose to implement the reasoner in Prolog, because of its efficiency, clarity, and familiarity. However, the logic used in Prolog is a somewhat awkward fit to the kind of open world reasoning that we want, as it does not support true negation and it makes the closed-world assumption. Thus, to express the non-occurrence of events, we have to use a work-around. We have to create a predicate `notOccurs(T1,T2,E)` to mean that event `E` does not occur in any interval overlapping `[T1,T2]`. Moreover, multiple versions of event functions must be created for different kinds of quantification of the variables.

For instance, suppose we want to assert that the state `outsideAt(O,L)` persists unless `O` is loaded into some container `OC`. One’s first thought might be to write this as

\[
persists(TA,T,\text{outsideAt}(O,L)) :- \text{notOccurs}(TA,T,\text{load}(O,OC)).
\]

but that, using Prolog’s negation as failure, will make the closed world assumption; it will succeed as long as it is cannot be inferred that `O` is loaded into some `OC`. We want to fail unless we know that `O` is not loaded into any `OC`.

There is no direct way around this in Prolog. Instead, we introduce a new predicate `notOccurs(T1,T2,E)`, meaning that we know that `E` does not occur in the interval `[T1,T2]`. But we are not yet out of the woods. The rule

\[
persists(TA,T,\text{outsideAt}(O,L)) :- \text{notOccurs}(TA,T,\text{load}(O,OC)).
\]

is still not right. The subgoal `notOccurs(TA,T,\text{load}(O,OC))` will succeed as long as it holds for any binding of `OC`. What this rule states is that `outsideAt(O,L)` persists as long as there is some container `OC` that `O` is not loaded into.

A third attempt

\[
persists(TA,T,\text{outsideAt}(O,L)) :- \forall \text{openContainer}(OC),\text{notOccurs}(TA,T,\text{load}(O,OC)).
\]

still does not work. This will loop through all the open containers that are explicitly mentioned in the problem specification; but in an open world we want to avoid excluding the possibility that `O` is loaded into to some unnamed container.

Instead, we must define a separate predicate “loadIntoSomething(O)” and state the rule as

\[
persists(TA,T,\text{outsideAt}(O,L)) :- \text{notOccurs}(TA,T,\text{loadIntoSomething}(O)).
\]

The corresponding constraint appears in the problem specification.

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2. It has been suggested that we would do better to use an open-world logic-programming language. In earlier studies (Davis, Marcus, & Frazier-Logue, 2017) we used the SPASS first-order theorem prover (Weidenbach et al., 2008) but we found that ineffective for complex chains of reasoning. Description logics typically have an open-world semantics, but do not seem to be expressive enough for our purposes. We will continue to look for other options; e.g. the system described in (e.g. Jackson, Schulte & Bjørner, 2013). However, for rapid prototyping, Prolog seemed a reasonable choice.
5.3 Incompleteness of Inference

The inference engine describe here is not, by any means, complete for the microworld; that is, there are inferences valid in the microworld that the inference engine cannot carry out.

For instance, in our microworld, given the two facts \( \text{occurs}(t_1, t_2, \text{carry}(o, la)) \) and \( \text{openContainer}(oc) \) it is in fact a consequence that \( \text{holds}(t_2, \text{notContained}(o, oc)) \); only top-level objects can be carried, so at time \( t_1 \), \( o \) is not contained in \( oc \), and this state persists through a carry action. But our inference methods do not include inferring that a precondition of an action holds from the fact that the action occurs.

6. Future Work

We plan to continue this project in a number of directions:

- Add functionalities of the reasoning systems
  - Reasoning about sets of objects in addition to individual objects.
  - Incorporating some degree of geometric reasoning.
  - Adding a front end that can take input from images.

- Characterize theoretically the power of algorithms and the difficulty of problems in this open-world reasoning.

- Run experiments to study this kind of reasoning in humans.

7. Conclusions

Intelligent action often requires reasoning that carried out in an “open world” in which an agent must come to conclusions based on knowledge that is significantly incomplete. By contrast, existing automated physical reasoning systems are almost all carry out reasoning that uses strong closed-world assumptions, in which initial states and exogenous events or actions are completely specified, relative to some As a step toward bridging this gap, we have developed, as a proof of concept, an initial version of an open-world reasoning system for a toy world of containers that includes actions with complex, recursive effects. Unlike most physical reasoners, the reasoning system can make inferences despite incomplete specifications of both the starting state and of the sequence of actions taken. The reasoning system has been implemented in Prolog. The inference procedure is not logically complete but it is sound, and works on our test examples of problems of moderate complexity. We plan to extend the system to richer physical theories and other forms of partial specification.

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