Noise reduction in ECG signals for bio-telemetry

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ABSTRACT

In Biotelemetry, Biomedical signal such as ECG is extremely important in the diagnosis of patients in remote location and is recorded commonly with noise. Considered attention is required for analysis of ECG signal to find the patho-physiology and status of patient. In this paper, LMS and RLS algorithm are implemented on adaptive FIR filter for reducing power line interference (50Hz) and (AWGN) noise on ECG signals. The ECG signals are randomly chosen from MIT_BIH data base and de-noising using algorithms. The peaks and heart rate of the ECG signal are estimated. The measurements are taken in terms of Signal Power, Noise Power and Mean Square Error.

Keywords:
ECG signals
LMS algorithm
Mean Square Error
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1. INTRODUCTION

The Electro Cardiogram (ECG) produces electrical signals of each cardiac cycle. In the cardiac cycle each event has its own significance to study the behaviour of patient cardiac pathophysiology. Generally ECG signals are Bio electrical signal which gives the electrical activity of heart versus time. Therefore it is very important to diagnose for analysing heart function [1]. The Bio electrodes are placed on the skin of the patient to acquire ECG signals. The pacemakers are located in the upper part of the right atrium. It fires electrical pulses to the nerves to stimulate the contraction phase. These pulses extend over the atrial walls and activate cardiac muscles to contract. The ECG and power-line signal’s frequency range is typically 0.05 to 100Hz and 50Hz so, ECG signals sensitive to the power line signals in the range around 50Hz which are causing interference [2]. 50Hz PLIN will interrupt the P and Q waves of the ECG signal. Most of Asian regions, Domestic and hospital power line are in the range of 50 Hz. So the frequency components associated in ECG that is 50 Hz are effected by the power line signals causing interference in ECG. But lack of power line quality the power signals are swings between the 47 to 53 Hz so the interference also effects from this range of power line signal. To mitigate this dynamic interference from power line we need use adaptive filter to suppress this random noise causing from power line [3]. An adaptive noise elimination filter has been used to evade this impending loss of information. Four different waves can be observed while recording ECG signal those are PQRST. The depolarization of right atria represents P wave. While the rapid depolarization of right and left ventricles represents QRS wave. The repolarization of the ventricles represents T wave [4], [5]. Any deviation in the said parameters leads abnormalities in the heart. The wave form related to QRS complex represent the contraction of left and right ventricles, which is more powerful than that of atria .It comprises muscle mass and causing a more ECG deflection. The Q wave signifies the signal horizontal (i.e. left to right) current as a potential travel through the inter-ventricular system. The Q wave is not having a septal origin shows myocardial violation which involves the full depth of
myocardium. The P wave arises when the SA node (Sinus Atria) generates a potential which depolarizes the atria. However as long as the atrial depolarization takes place to spread through the AV node to the ventricles, each p wave should be trailed by QRS complex [6]. From the commencement of QRS complex is called PR interval. This indicates the time that it takes for the electrical impulses produced in the SA node and to travel through the atria and across the AV node (Atria Ventricle) node to the ventricle. In adaptive filter, least mean square algorithm requires input signal and reference signal to update the (tap weights) filter coefficients of the adaptive FIR filter. For every iteration, LMS algorithm update new tap weights based on the previous tap weights to minimize the error. After several iterations, it eliminate the noise in the adaptive filter and gives best minimum mean square error. This method follows the computation based on the past available information. The RLS (recursive least square) algorithm gives better convergence than LMS algorithm [7]. The main disadvantage of the RLS algorithm is having high computational cost. In the paper, Section 2 shows the LMS and RLS algorithm, Section 3 gives the simulation results and Section 4 gives the conclusion results.

2. ADAPTIVE FILTERING

Adaptive filter involves the alteration of filter parameters (coefficient) over time to reduce the noise in the signal and to minimize the error [8]. Digital signal processing exhibited by most of the adaptive filters will be digital in nature because of complexity in optimizing algorithms. Adaptive filters are best suited when there is large uncertainty and filter has to compensate that or signal conditions are slowly changing. The performance of adaptive filter involves two process, which are filter processing and adaptation process [9].

The adaptive filter output Z(n) is given as:

\[ Z(n) = P(n)S(n) \]  

where S(n) is the input ECG signal and P(n) are the adaptive filter coefficients.

As we known ECG signal interference by 50 Hz power line signal. So, we have to suppress the 50 Hz component in the ECG signal which are originated by the power line. If we remove complete 50 Hz component in the ECG signal there may be data loss in the ECG signal which are associated with 50Hz frequencies region. So we need to estimate the disturbance by power line signal for that we giving power line signal as reference to the adaptive filter. Now the adaptive filter will track the power line components in ECG signal and we can easily extract interference part in the ECG signal. The difference between the desired signal d(n) and the signal from the output of the filter Z(n) is the error signal e(n).

\[ e(n) = d(n) - Z(n) \]  

The filter variable updates filter coefficients at every time instantaneous.

\[ P(n + 1) = P(n) + \Delta P(n) \]  

Where P(n+1) is the updated weight vector with the previous weight vector and \( \Delta \) is the correction factor depends on the value.

3. LEAST MEAN SQUARE ALGORITHM

These algorithms was suggested by Widrow and Hoff. They developed LMS from their studies of pattern recognition [10]. In the LMS algorithms, the correction applied to the above mentioned estimate includes product of three factors: the error signal e(n-1), the (scalar) step-size parameter (\( \mu \)) and the tap-input vector s(n-1). LMS algorithm is the best selection if we are dealing with adaptive digital circuits in this case a filter that reject the bands of signal those causes interference to the ECG [11]. The basic operation of LMS algorithm is the recursive updating nature of filter coefficients by the reference of error signal.

Each iteration of LMS involves three steps:

Filter output:

\[ Z[n] = \sum_{n=1}^{N-1} S[n]P[n] \]
Estimation error:
\[ e(n) = d(n) - Z(n) \] (5)

Tap-weight adaptation:
\[ P[n + 1] = P[n] + \mu S[n]e[n] \] (6)

d(n) is taken as desired signal and Z(n) is the output response of the adaptive filter equation 4 shows the output response of the Filter with input signal S(n) and filter coefficients P(n).

4. RECURSIVE LEAST SQUARE ALGORITHM

With supreme computational complexity, RLS is the fastest converging algorithm. It cancels maximum amount of noise by minimizing error with the fastest rate. So in this study, a tradeoff between computational complexity and convergence rate is done to attain the utmost noise free signal. The filter output and error function of RLS algorithm are shown in Equations (8) and (9).

\[ R(n) = \frac{\lambda^{-1}L(n-1)u(n-1)}{1 + \lambda^{-1}u^H(n-1)u(n)} \] (7)

Where R(n) is the vector gain, L(n) is the inverse correlation matrix, u(n) is the buffered input vector and \( \lambda^{-1} \) denotes the reciprocal of the exponential weighting factor. The filter output is:
\[ Z(n) = P^T(n - 1)u(n) \] (8)

Error signal:
\[ e(n) = d(n) - Z(n) \] (9)

The updated coefficients as shown in equation:
\[ P(n) = P(n - 1) + R^H(n)e(n) \] (10)
\[ P(n) = P(n - 1) + R^H(n)[d(n) - Z(n)] \] (11)
\[ P(n) = P(n - 1) + R^H(n)[d(n) - P^T(n - 1)S(n)] \] (12)

where \( R^H(n) \) is the gain constant, with a sequence of training data up to time, the RLS algorithm estimates the weight by minimizing the resulting cost [13].where u(n) is the input, and \( \lambda \) is the stabilization parameter.

5. RESULTS AND ANALYSIS

ECG signals are randomly taken from MIT_BIH data base i.e. (101,104,106,109,124) [14]-[16].The length of each ECG signal is restricted to 3600 samples. In LMS algorithm the mu is taken as 0.02 and in RLS algorithm lambda is taken as one randomly.Matlab is taken as a tool for simulations and noise is considered as Adaptive White Gaussian Noise (AWGN) with power line interference of 50Hz on ECG signal with less noise power. After de-noising using LMS and RLS algorithm, ECG signals peaks are estimated and results are compared with original signals without noise.

3.1 Implementation of LMS Algorithm by reducing channel Noise and reducing Power line interference of 50 Hz in ECG Signal Shown in Figure 1 to Figure 7 and Table 1 to Figure 10.
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Figure 1. ECG waveform from MIT-BIH database

Figure 2. Noise signal

Figure 3. ECG signal + noise
Figure 4. Noise removal in ECG Signal using LMS algorithm

Figure 5. (50Hz) Power Line Interference suppression using LMS Algorithm

Figure 6. Noise removal in ECG Signal using LMS algorithm
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Table 1. Channel noise reduction on ECG signal using LMS algorithm by considering interference of the same signal by ith different phase in the channel with mu=0.02 taken randomly

| Signals from MIT_BIH data base | ECG Signal Power (dB) | Noise Signal Power (dB) | Power of the Error Signal (dB) | Mean Square deviation (dB) |
|--------------------------------|-----------------------|-------------------------|-------------------------------|---------------------------|
| 101                            | -0.3339               | 0.0843                  | -8.9620                       | -21.2726                  |
| 104                            | -0.1954               | 0.1034                  | -8.7943                       | -21.0287                  |
| 106                            | -0.0922               | 0.0702                  | -8.6967                       | -21.0243                  |
| 109                            | -0.4866               | 0.0771                  | -9.1009                       | -21.0891                  |
| 124                            | -1.2148               | -0.032                  | -9.8297                       | -22.5220                  |

Table 2. Power line interference of 50Hz on ECG signal by reducing interference using LMS algorithm by considering interference of the same signal by the different phase in the channel

| Types of Signal from MIT_BIH data base | ECG signal Power (dB) | Noise signal Power (dB) | Power of the Signal and Noise (dB) | Power of the Error Signal (dB) | Mean Square deviation (dB) |
|----------------------------------------|-----------------------|-------------------------|-----------------------------------|--------------------------------|---------------------------|
| 101                                    | -0.3339               | -3.010                  | 5.6820                            | -2.9158                       | -29.044                   |
| 104                                    | -0.1954               | -3.010                  | 5.8206                            | -2.7737                       | -28.8041                  |
| 106                                    | -0.0922               | -3.010                  | 5.9218                            | -2.6680                       | -28.7976                  |
| 109                                    | -0.4866               | -3.010                  | 5.5267                            | -3.0627                       | -28.8639                  |
| 124                                    | -1.2148               | -3.010                  | 4.8011                            | -3.7882                       | -30.2965                  |

Table 3. Channel noise reduction on ECG signal using RLS algorithm by considering interference of the same signal by ith different phase in the channel with =1 taken randomly

| Signals from MIT-BIH Arrhythmia data base | ECG signal Power (dB) | Noise signal Power (dB) | Power of the signal and Noise (dB) | Power of the Error Signal (dB) | Mean Square deviation (dB) |
|------------------------------------------|-----------------------|-------------------------|-----------------------------------|--------------------------------|---------------------------|
| 101                                      | -0.3339               | -0.0467                 | 5.6879                            | -0.0274                        | -29.044                   |
| 104                                      | -0.1954               | -0.0472                 | 5.8206                            | -0.0581                        | -28.8041                  |
| 106                                      | -0.0922               | -0.1854                 | 5.9218                            | -0.0630                        | -28.7976                  |
| 109                                      | 0.4866                | -0.2264                 | 5.5360                            | 0.0268                         | -30.2965                  |
| 124                                      | -1.2148               | -0.0494                 | 4.8114                            | 0.0065                         | -30.2965                  |

Table 4. Power line interference of 50Hz on ECG signal by reducing interference using RLS algorithm by considering interference of the same signal by the different phase in the channel

| Signal from MIT-BIH data base | Power of the original ECG signal (dB) | Noise signal Power (dB) | Power of the Signal and Noise (dB) | Power of the Error Signal (dB) |
|-------------------------------|--------------------------------------|-------------------------|-----------------------------------|--------------------------------|
| 101                           | -0.3339                              | -3.010                  | 5.6879                            | -0.0274                        |
| 104                           | -0.1954                              | -3.010                  | 5.8274                            | -0.0581                        |
| 106                           | -0.0922                              | -3.010                  | 5.9320                            | -0.0630                        |
| 109                           | -0.4866                              | -3.010                  | 5.5360                            | 0.0268                         |
| 124                           | -1.2148                              | -3.010                  | 4.8114                            | 0.0065                         |

Table 5. Estimation signal power in time and frequency domain for the Signals from MIT-BIH

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Signals from MIT-BIH Arrhythmia data base | Power Time domain (dB) | Power Frequency domain (dB)
---|---|---
101 | -0.3272 | -0.3938
104 | -0.1932 | -0.1920
106 | -0.0886 | -0.0801
109 | -0.4845 | -0.5635
124 | -1.2092 | -0.9733

Table 6. Each ECG signal’s length is having 3600 samples under noise less conditions, QRST peaks are estimated in ECG signals as shown in the table (mV)

| Signal from MIT-BIH data base | R Peak (mV) | S Peak (mV) | T Peak (mV) | Q Peak (mV) | Heart Rate beats/min |
|---|---|---|---|---|---|
| 101 | 203.23 | -25.535 | 35.965 | -6.672 | 45.83 |
| 104 | 266.12 | 3.458 | 259.47 | 141.616 | 58.33 |
| 106 | 355.24 | -26.902 | 145.803 | 115.92 | 54.16 |
| 109 | 256.372 | -23.832 | 208.24 | 163.611 | 66.66 |
| 124 | 390.59 | -41.245 | 20.3103 | 102.8 | 33.33 |

Table 7. LMS algorithm is taken on noisy ECG signals which are corrupted with additive white gaussian noise. QRST peaks are measured (mV)

| Signals from MIT-BIH data base | R Peak (mV) | S Peak (mV) | T Peak (mV) | Q Peak (mV) | Heart Rate beats/min |
|---|---|---|---|---|---|
| 101 | 75.65 | -9.469 | 13.200 | -2.706 | 45.83 |
| 104 | 98.99 | 1.317 | 96.503 | 52.671 | 58.33 |
| 106 | 132.36 | -9.690 | 54.309 | 42.87 | 54.16 |
| 109 | 94.71 | 8.86 | 77.436 | 61.396 | 66.66 |
| 124 | 145.15 | -15.42 | 7.398 | 38.233 | 33.33 |

Table 8. LMS algorithm is introduced on signal of ECG to minimize the 50Hz power line interference on ECG system for considering \( \mu = 0.02 \). The readings are taken in terms of milli volts as shown in the table

| Signal from MIT-BIH Arrhythmia data base | R Peak (mV) | S Peak (mV) | T Peak (mV) | Q Peak (mV) | Heart Rate beats/min |
|---|---|---|---|---|---|
| 101 | 75.745 | -9.571 | 13.242 | -2.392 | 45.83 |
| 104 | 98.855 | 1.691 | 96.343 | 52.503 | 58.33 |
| 106 | 132.288 | -9.827 | 54.395 | 42.822 | 54.16 |
| 109 | 96.264 | 8.813 | 77.511 | 61.396 | 66.66 |
| 124 | 144.994 | -15.207 | 7.584 | 38.137 | 33.33 |

Table 9. RLS algorithm is taken on noisy ECG signals to reduce AWGN noise on the noisy ECG signals. Readings are taken for different signals in MIT data base and measurements are in milli volts

| Signal from MIT-BIH Arrhythmia data base | R Peak (mV) | S Peak (mV) | T Peak (mV) | Q Peak (mV) | Heart Rate beats/min |
|---|---|---|---|---|---|
| 101 | 0.2089 | -0.0275 | 0.036 | -0.0035 | 45.83 |
| 104 | 0.2660 | 0.0032 | 0.2702 | 0.1406 | 58.33 |
| 106 | 0.3412 | -0.0299 | 0.1447 | 0.1056 | 54.16 |
| 109 | 0.2623 | 0.0272 | 0.2142 | 0.1611 | 66.66 |
| 124 | 0.4459 | -0.0472 | 0.0246 | 0.1154 | 33.33 |

Table 10. RLS algorithm is considered to remove power line interference on the ECG signals which are interfered with 50Hz power line frequency in the system.

By observing Table 6 to Table 10 power line interference (50Hz) in the system and noise in the channel are suppressed to maximum extend using LMS and RLS algorithm. The peaks of QRST in ECG waves and heart rates are measured for different signals from MIT _BIH data base.
6. CONCLUSION

In this paper, the ECG signals are taken from physio-net for analysis. For Bio-telemetry applications, signals are transmitted from remote locations, LMS and RLS adaptive algorithms are considered for suppression of AWGN noise and power line interference on ECG signals. The analysis is carried out to evaluate the ECG signal power, noise signal and Mean square error. It is observed that Mean square error is less in RLS than LMS. Noise cancellation capacity is good in RLS than LMS. But the implementation is complex over LMS. After denoising at the receiver end, QRST peaks and heart beats are estimated and compared with the original QRST peaks and heart beats.

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