Shielding Dynamic Magnetic Fields to Sub-nT Levels in Linear Colliders

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Abstract

There is an increasing need to shield beams and accelerator elements from stray magnetic fields. The application of magnetic shielding in linear colliders is discussed. The shielding performance of soft iron and mu-metal is measured for magnetic fields of varying amplitude and frequency. Special attention is given to characterise the shielding performance for very small-amplitude magnetic fields.

1 Introduction

Magnetic fields can influence the operation of an accelerator. This could be a direct impact on the beam or an influence on accelerator elements. Linear colliders (described below) have an unprecedented sensitivity to external dynamic (stray) magnetic fields.

1.1 Linear Colliders

The luminosity of a linear $e^+e^-$ collider is [1]

$$L = \frac{N^2 f_{\text{rep}} n_b}{4\pi \sigma_x^* \sigma_y^*} H_D,$$

where $N$ is the bunch population, $f_{\text{rep}}$ is the repetition frequency, $n_b$ is the number of bunches, $\sigma_x^*$ ($\sigma_y^*$) is the horizontal (vertical) beam size at the interaction point and $H_D$ is a luminosity enhancement factor due to the electromagnetic interaction between the colliding bunches.

To achieve a large luminosity extremely small vertical beam sizes are targeted. The small vertical beam size leads to a sensitivity to stray magnetic fields, which can deflect the beams and result in a relative offset at collision. The Compact Linear Collider (CLIC)
is sensitive to stray magnetic field amplitudes of 0.1 nT [4, 5, 6, 7, 8] and the International Linear Collider (ILC) is sensitive to stray magnetic field amplitudes of 1 nT [9]. Ambient magnetic fields in accelerator environments exhibit fluctuations on the level of 100 nT [8, 10]. Therefore to mitigate performance loss, a mitigation system will be essential.

There are two options for such a system: an active compensation device or a passive shielding system. An active compensation device would measure the magnetic field and use a set of coils to compensated it. Such a device was demonstrated at an accelerator facility in [11]. This system stabilised a magnetic field to fluctuations of less than 10 nT. However, an active compensation device relies on accurately measuring the magnetic field. Measuring magnetic field fluctuations of 0.1 nT is challenging with current commercially available magnetometers [12]. Therefore, a passive shielding system is preferred. A shielding factor of approximately $10^3$ is required to reduce a 100 nT stray magnetic field to the level of 0.1 nT.

2 Magnetic Shielding

This section describes the current use of magnetic shields in linear colliders and the properties that affect shielding performance.

2.1 Applications in Linear Colliders

The most common use for magnetic shields in linear colliders is for superconducting radio-frequency (SRF) cavities, which are used in the ILC [9]. SRF cavities must be cooled down to superconducting temperatures to operate, usually 2 K. If magnetic flux is trapped inside the cavity walls during the cool down the quality factor of the cavity is reduced [13]. A magnetic shield is used to prevent magnetic flux trapping. Studies of potential magnetic shields for ILC SRF cavities are presented in [14, 15, 16].

In the above application, the magnetic shield is used to shield static magnetic fields. In this work, we look at the use of magnetic shields to shield the beam from dynamic magnetic fields. In particular, low-frequency small-amplitude magnetic fields.

2.2 Shielding Mechanisms and Magnetic Permeability

An overview of magnetic shielding is given in [17]. There are two magnetic shielding mechanisms, which are shown in Figure [1]. On the left is the flux-shunting mechanism, which is effective for shielding static and low-frequency magnetic fields, and on the right is eddy-current cancellation, which is only effective for high-frequency magnetic fields. In CLIC it is necessary to shield low-frequency magnetic fields, therefore the flux-shunting mechanism is of interest.

The flux-shunting mechanism relies on the material possessing a large permeability to draw the magnetic field away from the shielded region. Ferromagnetic materials [18] are commonly used for this purpose. The permeability of a ferromagnetic material that is exposed to a dynamic magnetic field is given by

$$\mu(H) = \frac{B(H)}{H}.$$ (2)
where $H$ is the amplitude of the magnetic field variations and $B(H)$ is the amplitude of the magnetic induction. The permeability is independent of a static offset provided the material is not close to saturation.

The response of a material to a small-amplitude dynamic magnetic field is governed by Rayleigh’s law, which states the amplitude of the magnetic induction is given by

$$B(H) = \mu_i H + \nu H^2,$$

(3)

where $\mu_i$ is the initial permeability and $\nu$ is Rayleigh’s constant. The permeability in the Rayleigh region is given by

$$\mu(H) = \mu_i + \nu H.$$

(4)

In order to effectively shield small-amplitude magnetic fields, the material must possess a sufficiently high initial permeability.

### 3 Measurements

Two ferromagnetic materials were characterised: soft iron and a nickel-iron alloy known as mu-metal. The magnetic shielding performance is measured with a transfer function, which is described below.

#### 3.1 Transfer Functions

Considering a magnetic shield exposed to the time-varying magnetic field $H_\text{e}e^{j2\pi ft}$, where $f$ is the frequency, $t$ is the time, $H_\text{e}$ is the external magnetic field amplitude and $j = \sqrt{-1}$, the magnetic field in the shielded region is $H_\text{e}e^{j(2\pi ft - \phi)}$, where $\phi$ is a phase shift introduced by the shield and $H_\text{e}$ is the internal magnetic field amplitude. The transfer function of the magnetic shield is given by

$$T(f) = \frac{H_\text{i}e^{-j\phi}}{H_\text{e}},$$

(5)

The absolute value of $T(f)$ is known as the amplitude response and the phase of $T(f)$ is known as the phase response.

For simple geometries, such as an infinitely long cylinder, analytical solutions to Maxwell’s equations exist for the propagation of electromagnetic waves through magnetic shields. A method for calculating the shielding factor of cylindrical shields is described in [20].
3.2 Methodology

A cylinder of inner diameter 5 cm, thickness 1 mm and length 50 cm was formed from soft iron and another cylinder with the same dimensions were formed from mu-metal. Both cylinders were annealed in their final form. The advertised magnetic properties of each material (provided by the supplier) are summarised in Table 1.

| Property                  | Soft Iron | Mu-Metal |
|---------------------------|-----------|----------|
| Initial permeability      | 300-500   | 50,000   |
| Maximum relative permeability | 3,500-8,000 | 250,000 |
| Magnetic induction at saturation | 2.15 T     | 0.74 T   |

Table 1: Advertised specifications of each material.

A three-axis Bartington Mag-13 fluxgate magnetometer [21] was used in measurements. The noise level of this sensor is low enough to measure magnetic field amplitudes of less than 0.1 nT. A set of Helmholtz coils [12] was used to generate a magnetic field excitation at a precise frequency and amplitude. A Mag-13 sensor was placed at the centre of the Helmholtz coils.

The magnetic field $H(t)$ was measured with and without a shield surrounding the sensor. In both measurements the current in the Helmholtz coils $I(t)$ was simultaneously recorded. A transfer function that relates the current in the Helmholtz coil to the magnetic field measured by the sensor was calculated:

$$T_{IH}(f) = \frac{P_{IH}(f)}{P_{II}(f)},$$

(6)

where $P_{IH}(f)$ is the cross power spectral density of $I(t)$ and $H(t)$ and $P_{II}(f)$ is the power spectral density of $I(t)$. The transfer function for the shield was calculated as

$$T(f) = \frac{T_{IH,sh}(f)}{T_{IH,no\ sh}(f)},$$

(7)

where $T_{IH,sh}(f)$ is the transfer function measured with the shield and $T_{IH,no\ sh}$ is the transfer function measured without the shield.

3.3 Soft Iron

The transfer function of a high purity (99.9%) iron cylinder was measured with different external magnetic field amplitudes. The transfer functions are shown in Figure 2. There is a clear dependence on the external magnetic field amplitude, where the shielding improves with the amplitude. The phase response of the iron cylinder is independent of the external magnetic field amplitude.

Figure 3 shows the measured amplitude response as a function of external magnetic field. It is clear the amplitude response tends to a constant as the external magnetic field is decreased.

The model described in [20] can be used to fit a permeability to the transfer function for each amplitude. Figure 4 shows the relative permeability as a function of external magnetic field amplitude. The initial permeability is extrapolated by fitting a straight line to the relative permeability. An initial permeability of $\mu_i = (204 \pm 5)$ was measured for this iron cylinder, which is somewhat below the advertised value of 300-500.
Figure 2: Transfer function of the iron cylinder for different external magnetic field amplitudes. Left: amplitude response $|T(f)|$ vs frequency $f$. Right: phase response $\angle T(f)$ vs frequency $f$. Error bars are too small to be seen.

Figure 3: Amplitude response of the soft iron cylinder $|T(H_e)|$ vs external magnetic field amplitude $H_e$ for different frequencies. Error bars too small to be seen.

3.4 Mu-Metal

The chemical composition of the mu-metal used was 80% Ni, 15% Fe, 4.5% Mo, 0.4% Mn and 0.1% Si. The transfer function of the mu-metal cylinder measured with different external magnetic field amplitudes is shown in Figure 5. The transfer functions appear to be similar.

Figure 6 shows the permeability fitted to each transfer function in Figure 5. There is a clear linear relationship between the permeability and external magnetic field amplitude. The relative change in permeability over the range measured is much smaller for the mu-metal compared to the iron. The initial permeability of the mu-metal cylinder is $\mu_i = (55,955 \pm 7)$, which is above the advertised value of $\mu_i = 50,000$.

3.4.1 Shielding to Sub-nT Magnetic Fields

CLIC has stray magnetic field tolerances down to 0.1 nT [4, 5, 6, 7, 8]. Realising this level requires a very effective magnetic shield with a sufficiently high initial permeability. A
Figure 4: Relative permeability of the soft iron cylinder \( \mu_r(H_e) \) vs external magnetic field amplitude \( H_e \): measurement (blue) and a straight line fit (orange). The errors bars were derived from fitting the model described in [20] to the transfer functions in Fig. 2.

Figure 5: Transfer function of the mu-metal cylinder for different external magnetic field amplitudes. Left: amplitude response \( |T(f)| \) vs frequency \( f \). Right: phase response \( \angle T(f) \) vs frequency \( f \). Error bars are too small to be seen.

0.1 nT internal magnetic field amplitude can be demonstrated with an external magnetic field amplitude of 1.1 \( \mu T \). This is shown in Figure 7. The expected amplitude of stray magnetic fields in accelerator environments is up to 100 nT \[8, 10\], which is an order of magnitude less than the excitation used in the measurement shown in Figure 7. Therefore, we can be confident that the stray field amplitude inside a mu-metal shield will be less than 0.1 nT for external amplitudes of 100 nT.

### 3.4.2 Mu-Metal Foils

Mu-metal is also available in thin foils, typically of thicknesses 0.1-0.5 mm. These foils are annealed and advertised as retaining their magnetic properties after slight deformation.

A set of three cylindrical shields of varying diameter \( D \) and thickness \( \Delta \) were formed from a mu-metal foil. The foil had the same chemical composition as the mu-metal cylinder discussed in the previous section. Figure 8 shows the transfer function of each shield formed from the mu-metal foil.
Figure 6: Relative permeability of the mu-metal cylinder $\mu_r(H_e)$ vs external magnetic field amplitude $H_e$: measurement (blue) and straight line fit (orange). The errors bars were derived from fitting the model described in [20] to the transfer functions in Fig. 5.

Figure 7: Internal magnetic field amplitude $H_i(f)$ of the mu-metal cylinder with an external magnetic field amplitude of 1.1 $\mu$T vs frequency $f$.

| Diameter, $D$ [cm] | Thickness, $\Delta$ [mm] | Relative Permeability, $\mu_r$ |
|-------------------|--------------------------|-----------------------------|
| 5.9 ± 0.2         | 0.1                      | 3,670 ± 2                   |
| 4.5 ± 0.2         | 0.2                      | 3,602 ± 2                   |
| 4.5 ± 0.2         | 0.1                      | 4,660 ± 50                  |

Table 2: Measured relative permeability of three shields formed from a mu-metal foil.

Table 2 shows the permeability fitted to each amplitude response. The foils have a relative permeability of less than 5,000, which is very poor for mu-metal. It is likely that the permeability was damaged by deforming the cylinder when rolling the mu-metal foil to produce the shield, this is discussed in Sec. 4.3.3.

A simple model for the shielding factor of a mu-metal shield is presented in [22]. For
a single layer, the amplitude response is given by

\[ T = \frac{D}{\mu_r \Delta}. \]  

This model does not include shielding via the eddy-current cancellation mechanism. For small external magnetic field amplitudes, the relative permeability in Eq. (8) is replaced with the initial permeability. The measured amplitude response for the different mu-metal foils is roughly consistent with Eq. (8).

4 Magnetic Shielding in Linear Colliders

This section describes various considerations for using the above materials to shield magnetic fields in linear colliders. The factors that affect shielding performance are also discussed.

4.1 Beam Pipes

A beam pipe is used to contain the vacuum in an accelerator. In linear colliders, they typically consist of a few millimetres of steel and a 10-100 \( \mu \)m inner copper coating to mitigate long-range wakefields.

The impact of stray magnetic fields can be mitigated by preventing them from reaching the beam. This can be achieved by surrounding the beam with a shield or surrounding the sources with a shield. The beam pipe is usually the closest component to the beam. Therefore, surrounding the beam pipe is the safest option because it prevents stray fields from all external sources reaching the beam. To shield the sources, they must first be identified and the feasibility of surrounding them with a shield must be studied.

Mu-metal is a good candidate material to wrap around the beam pipe. Since it could be wrapped around the beam pipe if deemed necessary after the accelerator has been constructed. Alternatively, a mu-metal layer could be incorporated into the beam pipe design and the entire beam pipe could be annealed in its final form, which would ensure a good shielding performance.
4.2 Magnets

Beam pipes are typically formed from non-magnetic materials because they run through the aperture of magnets. They should not impede the magnetic field generated by a magnet, which is used to guide the beam.

The sensitivity to stray magnetic fields in linear colliders comes from the long drifts between magnets. Therefore, only the drifts need to be shielded, which avoids the problem of shielding inside the magnets.

Large static magnetic fields saturate ferromagnetic materials. Once a material is saturated, it is no longer effective as a magnetic shield. Depending on the required internal field level, this property enables the possibility of replacing the steel in a beam pipe with soft iron. Inside a magnet the soft iron beam pipe will be saturated and will not impede the magnetic field, whereas in the drifts the soft iron beam pipe will shield the beam.

4.3 Factors Affecting Performance

Factors that affect the performance of magnetic shields are discussed in [23]. The factors that affect the shielding performance of dynamic magnetic fields are summarised below.

4.3.1 Saturation

Eq. (4) is valid provided a static magnetic field does not saturate the material. If the material is saturated, its permeability and shielding performance drops. Using Eq. (8) it is straightforward to show a mu-metal shield will not saturate provided

\[ B_s > \frac{D}{\Delta} H, \]  

where \( B_s \) is the magnetic induction at saturation. The magnetic induction for the mu-metal used in this work is \( B_s = 0.74 \) T (see Table 1). The dominant static magnetic field in an accelerator environment is typically the Earth’s magnetic field, which is approximately 20-70 \( \mu \)T [24]. Assuming 50 \( \mu \)T for the Earth’s magnetic field, this requires a shield geometry that satisfies \( D/\Delta < 15,000 \), which is easily achieved. The magnetic shields considered in this work have a \( D/\Delta \) between 10 and 1000.

Alternatively, an additional outer layer can be included in the shield, which has a higher magnetic induction at saturation, e.g. a nickel-iron alloy with a lower nickel content than mu-metal [25]. The outer layer will attenuate the static magnetic field and ensure an inner mu-metal layer does not saturate.

4.3.2 Annealing

Soft ferromagnetic materials are often annealed in a dry hydrogen environment after being bent into their final form. This removes impurities from the material and alters the crystal structure of the material, which allows magnetic domains to move freely [26, 27]. As a result, the permeability of the material is significantly increased [28, 29, 30].

4.3.3 Mechanical Stress, Deformation and Shock

It is well known that mechanical stress, deformation and shock can significantly reduce the permeability of a ferromagnetic material [31, 32]. The damage can be reversed by re-annealing the shield, which can increase the permeability by an order of magnitude [30].
Mu-metal requires hydrogen annealing at very high temperatures (above 1000°C) which means re-annealing in the accelerator tunnel impractical. The sample should be handled with care after annealing to avoid performance loss.

4.3.4 Temperature

It was observed in [15, 30] that the shielding factor of a mu-metal shield degrades at very low (superconducting) temperatures. This is only a concern for accelerators that operate at superconducting temperatures, such as the ILC. CLIC operates at room temperature, which means the degradation of shielding at low temperatures is not a concern.

5 Conclusions

The behaviour of the permeability for very small-amplitude magnetic fields (Rayleigh’s law) has been verified. It is possible to shield extremely small-amplitude magnetic fields, down to the level of 0.1 nT, with mu-metal. Mu-metal is sensitive to permeability loss from mechanical stress and deformation. It should be handled with care after annealing. A simple formula (Eq. (8)) was verified for calculating the transfer function of mu-metal.

There is an increasing need to shield beams in accelerators from external magnetic fields, in particular for future linear colliders. In this paper, we have confirmed experimentally that mu-metal is a viable material that can be used to shield dynamic magnetic fields to amplitudes of less than 0.1 nT. This is particularly important for CLIC which requires the stray fields experienced by the beam do not exceed 0.1 nT. A mu-metal shield has been included in the design of CLIC for this purpose [8].

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