Aging near rough and smooth boundaries in colloidal glasses

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(Dated: 24 July 2018)

We use confocal microscopy to study the aging of a bidisperse colloidal glass near rough and smooth boundaries. Near smooth boundaries, the particles form layers, and particle motion is dramatically slower near the boundary as compared to the bulk. Near rough boundaries, the layers nearly vanish, and particle motion is nearly identical to that of the bulk. The gradient in dynamics near the boundaries is demonstrated to be a function of the gradient in structure for both types of boundaries. Our observations show that wall-induced layer structures strongly influence aging.

I. INTRODUCTION

Glasses are solids with disordered structures and slow internal dynamics. Efforts to understand the influence of boundaries on glassy dynamics has been an active area of research for more than two decades \cite{10, 11, 30, 31, 37}. Initial efforts on confined systems were thought to provide a route to accessing postulated growing length scales associated with cooperative motion \cite{5, 9, 16}. However, the study of such small system sizes necessitates the presence of boundaries and it has turned out that the specific details of such interfaces have a great deal of influence on the local dynamics near the boundary. \cite{17} In experimental material systems, the type of interface often plays a dominant role over finite size effects where interfacial energy, specific chemical interactions, and substrate compliance are all factors that have shown to have some influence on the dynamics. \cite{18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29} In computer molecular dynamics (MD) simulations where the specific details of the boundary need to be constructed at its most basic level, it is unclear a priori how best to accomplish this.

Early MD efforts started with smooth, structureless walls where the boundary was treated as a continuum and details of the wall potential were integrated over in the lateral \((x,y)\) direction leaving only a \(z\)-dependence perpendicular to the boundary. \cite{2} Alternatively, molecularly structured walls assembled from Lenard-Jones (LJ) particles into either crystalline arrays or frozen amorphous structures were also investigated \cite{10, 11, 30, 31, 37}. In these simulations, local dynamic near the boundary were usually different than bulk, but the underlying cause why was frequently unclear. Smooth walls typically exhibit faster dynamics than bulk in part because there is no penalty for the particles to slide laterally along the wall \cite{9, 34, 35, 36, 37}, a type of motion only considered to be experimentally relevant for a free surface. \cite{36} Systems with molecularly structured walls, where lateral sliding is inhibited, typically exhibited slower dynamics in comparison \cite{10, 11, 13, 30, 31, 34}. One of the major challenges with such boundaries is that for mixtures of LJ particles or polymeric bead-spring models (the most commonly modeled systems), the presence of the wall creates layering of the particle density \(\rho(z)\) as a function of distance from the wall. \cite{2} Intuitively, the particles pack easily in a layer against the wall, and then the particles in the second layer pack against that first layer, etc., with the influence of the wall diminishing farther away. Thus, a major effort in these studies is the need to determine the extent to which the observed differences in local dynamics a distance \(z\) to the boundary are influenced by the local \(\rho(z)\) structure in density. In some cases slower dynamics near the boundary has been associated with a significantly increased local density \cite{5, 39}, while other studies have demonstrated that the change in dynamics near the boundary is unrelated to the \(\rho(z)\) density profile \cite{10, 11, 12, 13, 14, 15}. For example, even efforts to construct a neutral boundary that avoids local perturbations to the particle density by freezing in an amorphous, liquid-like structure still leads to perturbations in the local dynamics \cite{10, 11, 30, 39, 40, 41, 42}. It is important to note that local perturbations to the \(\rho(z)\) structure are not limited to only coarse-grained simulations, they are also observed in nearly-atomic, united-atom models. \cite{2} In addition, experimental studies on glassy thin film systems are also trying to uncover the extent to which molecular ordering occurs near a boundary and its possible influence on the local density and dynamics. \cite{45, 46, 47, 48, 49}

Here we present a direct experimental comparison of local glassy dynamics next to rough and smooth boundaries using colloidal glasses, which have been previously suggested as a means of experimentally verifying these observations from coarse-grained MD simulations of boundaries. \cite{5, 39, 50} Colloids are small solid particles in a liquid, where Brownian motion allows particles to diffuse and rearrange. \cite{2} We use confocal microscopy to study the aging of a bidisperse colloidal glass where layer-resolved dynamics as a function of distance from a rough or smooth wall are compared with the measured \(\rho(z)\) density profile. Smooth boundaries are simply a normal untreated glass coverslip, while rough boundaries are constructed by melting a small amount of the colloidal sample to the coverslip. These stuck particles cover approximately 30-50\% of the surface and provide a roughness scale comparable to the particle size. The particle-glass and particle-particle interactions are purely repulsive and so the main difference in the boundary con-

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ditions is the topography. We observe distinctly different results between smooth and rough boundary conditions: near smooth boundaries motion is dramatically slower, whereas near rough boundaries the aging process is nearly independent of the distance from the boundary. We ascribe this to the strong influence of layer-like structures formed near the smooth boundary.

Our samples are aging: unlike many phases of matter, glasses are out of equilibrium, and so their properties slowly evolve, perhaps toward a steady state. These properties can include the density, enthalpy, and diffusive motion of the molecules comprising the glass. This has implications for the usage of glassy materials which have properties that depend on age perhaps in an undesirable way. Aging has been observed in polymer glasses, granular systems, and soft materials such as colloids and foams. While for polymer glasses and granular materials aging is often measured as slight decreases in volume, colloidal glasses are typically studied at constant volume. The main signature of aging of colloidal glasses is the dramatic slowing of particle motion as the sample ages often characterized by the slowing down of the mean square particle displacement for time windows at increasing aging times. Previous work suggests that aging in colloidal systems may relate to the local structure around rearranging particles or domains of more mobile particles. In general, it is not surprising that confined glasses age in different ways from their bulk counterparts. In this manuscript we show that aging of colloidal particles is tied to layering structure imposed by the nearby sample boundaries.

II. EXPERIMENTAL DETAILS

In our experiment we use sterically stabilized poly(methyl methacrylate) (PMMA) particles to prevent aggregation. Two different sizes of particles are mixed in order to prevent crystallization, with \( d_1 = 2.52 \, \mu m \) and \( d_2 = 1.60 \, \mu m \). The particles have a polydispersity of 7%. The number ratio is approximately 1 : 1. To match the particles' density and refraction, we use a mixture of decalin and cyclohexylbromide as the solvent. We view our samples with a fast confocal microscope (VT-Eye from Visitech, International). The large particles are dyed with rhodamine dye and thus are visible, while the small particles are undyed and thus unseen. Based on prior work, we expect that both small and large particles have similar behaviors. Visual inspection using differential interference contrast microscopy, which can see both particle types, confirms that the particles are well-mixed even at the boundary. The imaged volume is \( 50 \times 50 \times 20 \, \mu m^3 \). These images are taken once per minute for 2 hours. Our scanning volume starts about 5 \( \mu m \) outside the boundary to ensure we have clear images of the particles at the boundary. The microscope pixel size is 0.11 \( \mu m \) in \( x \) and \( y \) (parallel to the boundary) and 0.2 \( \mu m \) in \( z \) (perpendicular to the boundary). We use standard software to track the motion of the particles in 3D. Our particle locations are accurate to 0.10 \( \mu m \) initially and to 0.15 \( \mu m \) by the end of the experiment after some photobleaching occurs.

We construct two types of sample chambers. The first uses a normal untreated coverslip as a smooth boundary. The second is prepared by taking a small amount of colloidal sample and melting this on to the coverslip, using an oven at 180° C for 20 min. After this process, the PMMA particles are irreversibly attached to the coverslip. This sample is the same bidisperse mixture of PMMA particles as the main sample with the exception that both particle sizes are undyed. By image analysis we determine that the stuck particles cover approximately 30-50% of the surface. The specific fraction is difficult to measure as we only image the large fluorescently dyed particles, so we cannot see either the smaller mobile particles of our bidisperse sample or the stuck particles of either size. After adding the samples, we never observe any of our sample particles stuck to the boundaries for either smooth or rough boundary conditions.

We add a stir bar inside each sample chamber so that we can shear rejuvenate the samples and thus initiate the aging process and set \( t_{age} = 0 \) (when we stop stirring). Note that \( t_{age} \) is set by the laboratory clock and thus is identical throughout our sample; we are not considering the idea of a spatially varying time scale. We find the stirring method gives reproducible results similar to prior work, although this is probably different from a temperature or density quench as is usually done for polymer and small molecule glasses. Given the flows caused by the stirring take 20-30 s to appreciably decay after stirring is stopped, there is some uncertainty in our \( t_{age} = 0 \), but we examine the data on time scales at least ten times larger than any uncertainty of this initial time.

Confocal microscopy allows us to measure the bulk number density for large particles, which we find to be \( 0.32 \pm 0.03 \, \mu m \). The uncertainty represents the variability that we see from location to location. Given that we cannot directly observe the small particles, the observed number density in any given location is not a useful measure of the local volume fraction. Thus, we do not have a direct measure of the volume fraction. Given that the samples behave as glasses (to be shown below) and particles are still able to move, we conclude \( \phi_{glass} < \phi < \phi_{rep} \), with \( \phi_{glass} \approx 0.58 \) (for bidisperse colloidal glasses) and \( \phi_{rep} \approx 0.65 \) (the value for random close packing for our bidisperse sample). Prior studies of aging colloidal glasses found little or no dependence of the behavior on \( \phi \). It is important to note that we cannot definitely establish if our two samples are at the same \( \phi \) or, if not, which one would be higher.

III. RESULTS

Figure 1 shows reconstructed 3D images for smooth (a) and rough (b) boundaries. To show the influence of
the boundaries, the particles closest to the boundary are on the top of these pictures (colored dark purple). The color changes continuously as a function of the distance $z$ away from the boundary. However, the particles shown in Fig. 1(a) appear to have discrete colors as they form layers with distinct $z$ values. This phenomena is induced by the flat wall and is well known\textsuperscript{27,28}.

To quantify the layered structure we measure the time-averaged number density for the large particles $n(z)$. This is shown in Fig. 2 for smooth (a) and rough (b) boundaries. We set $z = 0$ at the center of the particle whose center is closest to the boundary. The vertical dotted lines indicate the separate layers. As the sample is composed of two sizes of particles, the layer structure decreases rapidly away from the wall, consistent with simulations\textsuperscript{27,28} and experiments\textsuperscript{22}. The first peak in Fig. 2(a) has the maximum value and minimum width, indicating particles are in a well-defined layer, consistent with Fig. 1(a). By the sixth layer, it is unclear if there is still a layer or if we are seeing random number density fluctuations. For the rough wall in panel (b), the layers become poorly defined by the fourth layer. For later analysis, we continue counting the layers by defining them in the bulk region to be every 1.8 $\mu$m based on the typical spacing of the well-defined layers. Note that for the rough boundary condition, the wall texture occupies some of the space of the first layer, thus decreasing the number of dark purple particles in Fig. 1(b) and reducing the area under the first peak in Fig. 2(b).

Aging manifests as a slow change of sample behavior with increasing $t_{\text{age}}$, where the rate of change slows at longer times\textsuperscript{21}. The easiest quantity to see this with our data is the mean square displacement (MSD) of particle motion\textsuperscript{63,67}. Fig. 3 shows the motion parallel to the boundaries for (a,b) rough and (c,d) smooth boundaries, with panels (b) and (d) corresponding to the bulk MSD curves. The different colors indicate different ages. The mean square displacement is computed as $\frac{1}{3}(\Delta x^2 + \Delta y^2 + \Delta z^2)$ where the angle brackets indicate an average over all large particles and over all starting times within the window of $t_{\text{age}}$. For our shortest time scale ($\Delta t = 1$ min) the MSD curves have a shallow slope indicating particles are trapped by the local configuration, with the exception of the black curves ($t_{\text{age}} \leq 8$ min) when the aging has just started. At long time scales, the MSDs show an upturn, which is related to the samples' age\textsuperscript{62,63,67}. For larger $t_{\text{age}}$ the lag time particles need to reach the same MSD increases, indicating the slowing particle motion. Note that as we take data, the fluorescent dye in the particles begins to photobleach and our particle tracking resolution worsens, slightly increasing the measured MSD values at small $\Delta t$.\textsuperscript{79} Slight differences in image quality may also be affecting the overall height of the MSD curves between the smooth and rough boundary conditions for the data at $\Delta t \leq 10$ min\textsuperscript{79} According to previous analysis below, we will focus on large $\Delta t$ values for which the signal is greater than the photobleaching noise. The main points to learn from Fig. 3 are that the overall behavior of the curves shows the expected aging trend with larger $t_{\text{age}}$, and panels (b,d) show the aging curves are similar for both boundary conditions far from the boundary.

Figure 3(a) shows the MSD curves for $xy$ motion for the first layer with rough boundary conditions. Surprisingly, there barely exists any differences comparing to Fig. 3(b), which depicts the MSDs of the fourth layer. The particles overall show aging behavior with slower dynamics for larger $t_{\text{age}}$. In contrast to the rough boundary, the MSD curves for the first layer next to the smooth boundary look strikingly different from the bulk case, as seen by comparing Fig. 3(c) and (d). In all four time
The mean square displacement for motion parallel to the boundaries calculated as $\Delta r_{xy}^2 = \frac{1}{2} (\Delta x^2 + \Delta y^2)$. The data are averaged over four different $t_{age}$ regimes as indicated. Data are for (a) 1st layer with a rough boundary, (b) 4th layer with a rough boundary, (c) 1st layer with a smooth boundary, (d) 4th layer with a smooth boundary. The data for the 4th layers match the bulk behavior, and their progression to larger time scales with increasing $t_{age}$ demonstrates that the sample is aging. The data for the 1st layers show that aging is fairly unchanged for the rough boundary (a), but markedly different for the smooth boundary (c). All displacements are normalized by the large particle diameter $d_L$.

Figure 4 shows the MSD data for the $z$ component of motion, perpendicular to the boundary. The results are similar to the MSD data of Fig. 3, with the exception that the layers closest to the boundaries show less motion [panels (a,c)] for both rough and smooth boundary conditions. The increase in the height of the MSD curves with age in Fig. 4 is due to photobleaching, but otherwise those MSD curves are fairly flat. Here the first layer for the rough boundary shows some differences with the bulk behavior [compare panels (a) and (b)]. The contrast between first layer and bulk is stronger for the smooth boundary condition [compare panels (c) and (d)].

To better understand the influence of the boundaries, we consider a complementary analysis, examining $\langle \Delta r^2 \rangle$ at a fixed $\Delta t$ and varying $t_{age}$. We choose $\Delta t = 20$ min, where Figs. 3,4 show that the particles’ average movement decreases with increasing $t_{age}$ in both smooth and rough boundaries. Figure 5 shows the data divided by rough boundary condition (panels a,b) and smooth boundary condition (panels c,d), for motion parallel and perpendicular to the boundaries (left and right panels respectively). The colors indicate different layers, as labeled in panels (e,f). The overall decreasing trend of all the curves with larger $t_{age}$ is the signature of aging, with the logarithmic $t_{age}$ axis making apparent that the rate of decrease itself is slower in older samples. The data suggest the sample is still aging at the longest times observed in our experiment, although even reaching a state-steady for $\Delta t = 20$ min does not preclude the sample from still
having an aging signal at longer $\Delta t$.

For the rough boundaries [Fig. 5(a,b)], the data collapse for all layers confirming that the boundary appears to have a negligible influence on the dynamics. However, for the smooth boundary condition, the wall-induced structures bring significant differences for motion parallel to the boundary [Fig. 5(c)] and even larger differences in the perpendicular direction [Fig. 5(d)]. Both types of motion are slower closer to the wall. For the motion perpendicular to the boundary (panel d), the motion in the first layer is around ten times smaller than the bulk. Moreover, unlike other layers, we do not observe an aging signal in the first layer – the curve is essentially flat. The lack of observed aging behavior of $\Delta z^2$ suggests that this first layer has very slow dynamics. Of course, the perpendicular motion in the first layer is bounded at $z = 0$, but the displacements we observe are much smaller than for the first layer next to the rough wall, which has a similar constraint on perpendicular motion. Our observations of nearly immobile particles with no aging signature in this first layer matches results from thin polymer films near attractive silica substrates.21

As a different way of understanding how the aging process changes near the smooth boundary, we normalize $\langle \Delta r^2(t) \rangle$ by $\langle \Delta r^2(t_{\text{age}} = 1 \text{ min}) \rangle$ as shown in Fig. 5(e,f). For both motion parallel and perpendicular to the boundary, the data collapse moderately well for $t_{\text{age}} \lesssim 10$ min, indicating an initial aging trend. For $t_{\text{age}} \gtrsim 10$ min, the first and second layers nearly stop evolving while the other layers are still aging. This is especially true for the $z$ motion (panel f).

To further explore the relation between the layering structures and motion perpendicular to the boundary we define $\langle \Delta z^2_{\text{asym}} \rangle$. This is the average of the data of Fig. 5(b,d) in the asymptotic regime, that is, for $t_{\text{age}} \gtrsim 85$ min. The results are plotted as a function of the distance from the wall in Fig. 5(a). The smooth data (red circles) smoothly increases as $z$ increases. The rough data (blue triangles) are fairly constant, with the exception of the first layer ($z = 0.8 \mu m$) which is larger. As argued above based on the flatness of the data in Fig. 5(a), this increase in the first layer is likely due to photobleaching than true motion. For $z > 5 \mu m$ the differences between smooth and rough data are likely due to image quality which artificially increases the MSD.28 To account for this, in Fig. 5(b) the data are normalized by the value of $\langle \Delta z^2 \rangle$ averaged over $t_{\text{age}} \leq 5$ min. This collapses the data for $z > 5 \mu m$. These data are related to the amount of the dynamics slow as the sample ages, with 1 corresponding to no slowing and smaller values indicating slowing with age. The value close to 1 for the smooth boundary condition indicates that the first layer barely ages, consistent with the similarity of the MSD data of Fig. 5(c) and the horizontal red line in Fig. 5(d). The decrease in the data of Fig. 5(b) as $z$ increases shows a return to the normal aging seen in the bulk.

The qualitative similarity of the rough and smooth data in Fig. 5(b) motivate an attempt to collapse the data by a horizontal shift. Noting that the number density data of Fig. 5(b) look like a horizontally shifted portion of the data of Fig. 5(a), we use the local layer structure as a possible way to explain the dynamical data. We quantify the structure using the standard deviation of number density $\sigma_n$ over the mean number density $\langle n \rangle$ where these quantities are defined within each layer (see Fig 2). The data for the vertical coordinate correspond to that of Fig. 5(b).

FIG. 6 (a) The $t_{\text{age}}$ average of $\Delta z^2$ for the last 15 min of Fig. 5(b,d) plotted as a function of $z$, with the average done over all particles in a layer (as defined in Fig. 2). The $z$ value is the center of each layer over which the average is taken. (b) The same data normalized by the mean value of $\Delta z^2$ for $t_{\text{age}} \leq 5$ min. This represents the slowing seen due to aging: the data close to 1.0 show little or no aging behavior. The error bars represent the variability in the results when different ranges for the $t_{\text{age}}$-averaging are used.

FIG. 7 The large $t_{\text{age}}$ motion in $z$ plotted as a function of the standard deviation of number density $\sigma_n$ over the mean number density $\langle n \rangle$ where these quantities are defined within each layer (see Fig 2). The data for the vertical coordinate correspond to that of Fig. 5(b).
IV. CONCLUSIONS

In our experiment we study aging by observing particle motion in a colloidal glass near smooth and rough boundaries. Both samples exhibit aging in their bulk. Near a smooth boundary, the particles form layers against the boundary such that in the two layers closest to the wall, motion is greatly diminished. For a smooth wall, we observe the influence of the boundary extends up to $\approx 6$ layers ($\approx 4$ large particle diameters) into the sample. The observations of a gradient in dynamics near the smooth wall are qualitatively similar to prior observations of gradients near interfaces in glassy materials. Direct evidence for gradients in dynamics has been seen in molecular dynamics simulations and colloidal experiments. In other experiments the influences of the boundaries are inferred from local probes near the boundary (e.g., Ref. 24) or fitting the data to models assuming boundary effects (e.g., Ref. 25).

Here we not only see the gradient in dynamics, but observe that this gradient in dynamics is directly related to a gradient in the structural properties. For a rough boundary, the wall-induced structure is greatly reduced and the dynamics appear more bulk-like near the boundary, being similar to that far into the bulk. By comparing the local dynamics near the rough and smooth boundaries, our results suggest that the dominant factor modifying aging dynamics near a boundary is the structure caused by the presence of the boundary. By presenting a rough amorphous boundary, the structure is more bulk-like and thus the dynamics are more bulk-like. A fruitful area for future work would be to explore boundary textures that have intermediate influences on layering structure.

These experimental results on colloidal glasses suggest a viable means by which neutral rough amorphous boundaries may be implemented in computer simulations. This is an issue that computational studies on the influence of interfacial effects on local dynamics have been struggling with for more than two decades and has relevance for the implementation of theoretical point-to-set studies. The method employed in the present study creates a rough amorphous boundary by randomly sticking particles to a smooth wall at approximately 30–50% surface coverage. The local aging dynamics we observe near such a rough boundary appear nearly bulk-like with little deviation from bulk particle densities.

This work was supported by the National Science Foundation (DMR-1609763).

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