Long-term X-ray variability of Swift J1644+57

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ABSTRACT
We studied the X-ray timing and spectral variability of the X-ray source Sw J1644+57, a candidate for a tidal disruption event. We have separated the long-term trend (an initial decline followed by a plateau) from the short-term dips in the Swift light curve. Power spectra and Lomb–Scargle periodograms hint at possible periodic modulation. By using structure function analysis, we have shown that the dips were not random but occurred preferentially at time intervals \(\approx (2.3, 4.5, 9) \times 10^5\) s and their higher order multiples. After the plateau epoch, dipping resumed at \(\approx (0.7, 1.4) \times 10^6\) s and their multiples. We have also found that the X-ray spectrum became much softer during each of the early dips, while the spectrum outside the dips became mildly harder in its long-term evolution. We propose that the jet in the system undergoes precession and nutation, which causes the collimated core of the jet briefly to go out of our line of sight. The combined effects of precession and nutation provide a natural explanation for the peculiar patterns of the dips. We interpret the slow hardening of the baseline flux as a transition from an extended, optically thin emission region to a compact, more opaque emission core at the base of the jet.

Key words: accretion, accretion discs – black hole physics – methods: data analysis – galaxies: active – galaxies: jets – X-rays: individual: Sw J1644+57.

1 INTRODUCTION
Swift J164449.3+573451 (hereafter Sw J1644+57) was discovered by the Swift Burst Alert Telescope (BAT; Gehrels et al. 2004; Barthelmy et al. 2005) on 2011 March 28 (Burrows et al. 2011; Cummings et al. 2011). The long duration of the X-ray emission and flaring events (still ongoing after one year), and the spatial coincidence with the nucleus of a galaxy at redshift \(z = 0.354\) (luminosity distance \(\approx 5.7 \times 10^{27}\) cm; Levan et al. 2011a,b; Thoene et al. 2011) made it clear that it was not a gamma-ray burst, and was instead associated with some kind of sudden accretion event on to a supermassive black hole (BH; Bloom et al. 2011b; Burrows et al. 2011; Levan et al. 2011a). In particular, the precise position from Very Large Array and Very Long Baseline Array radio observations clinched the identification of the X-ray source with the nucleus of the host galaxy (Zauderer et al. 2011). The lack of previous evidence of nuclear activity (active galactic nucleus, AGN) from the same source, and the short time-scale for the outburst rise (a few days; Krimm & Barthelmy 2011), are difficult to reconcile with changes in the large-scale accretion flow through an accretion disc, but this scenario is not completely ruled out (Burrows et al. 2011). The most favoured scenario is a tidal disruption event deep inside the sphere of influence of the BH (Bloom et al. 2011a,b; Burrows et al. 2011; Cannizzo, Troja & Lodato 2011; Barres de Almeida & De Angelis 2011; Socrates 2012). The nature of the star being disrupted, and therefore the radius at which the event occurs and the time-scale on which the stellar material circularized into a disc and accreted are still matters of intense debate. For example, it was argued that if the disrupted star were a white dwarf, the smaller tidal disruption radius and characteristic time-scale would be more consistent with the observed duration of the flares (Krolik & Piran 2011).

There are no direct measurements of the BH mass (\(M_\bullet\)). Indirect order-of-magnitude constraints consist of an upper limit to the BH mass that permits tidal disruption events outside the event horizons (Rees 1988), a minimum variability time-scale of \(\sim 100\) s that sets an upper limit to the light-crossing time-scale (Bloom et al. 2011b; Burrows et al. 2011), and well-known empirical relations between \(M_\bullet\) and the host galactic environment (whatever causes those trends; e.g. Silk & Rees 1998; Jahnke & Macciò 2011). For example, based on the optical luminosity of the host galaxy, Levan et al. (2011a) estimate a spheroidal stellar mass of \(M_\text{sph} \sim 10^7 – 10^8 M_\odot\). Using the log-linear spheroidal mass–BH mass relation of Bennett et al. (2011) (see also Magorrian et al. 1998; Lauer et al. 2007; Kormendy, Bender & Cornel 2011), this implies a likely BH mass of \(2 \times 10^6 \lesssim M_\text{BH} \lesssim 10^7 M_\odot\) (Levan et al. 2011a); adopting instead the bent \(M_\text{sph} – M_\text{BH}\) relation of Graham (2012), it also allows a lower range of BH masses, \(10^5 \lesssim M_\text{BH} \lesssim 10^6 M_\odot\). The latter range is more consistent with the BH mass log\((M_\bullet/M_\odot) = 5.5\pm1.1\).
estimated by Miller & Gültekin (2011), based on empirical ‘Fundamental Plane’ relations between radio and X-ray luminosities of accreting BHs.

The relatively small BH mass implies a bolometric Eddington luminosity of \( \lesssim 10^{47} \, \text{erg} \, \text{s}^{-1} \), and a 0.3–10 keV luminosity a few times smaller. The average isotropic luminosity in the 0.3–10 keV band was \( \approx 10^{47} \, \text{erg} \, \text{s}^{-1} \) in the first few weeks after the initial outburst; several months (\( \approx 10^3 \) s) later, it was still \( \approx 100 \times 10^{45} \, \text{erg} \, \text{s}^{-1} \), well above the Eddington limit. This is strong evidence that the emission is beamed towards us (Bloom et al. 2011b; Burrows et al. 2011; Levan et al. 2011a), and is probably associated with a relativistic jet (Lei & Zhang 2011), like in blazars. A relativistic jet has also been invoked to explain the radio transient event, interpreted as an external shock in the gas surrounding Sw J1644+57 (Bower, Bloom & Cenko 2011; Burrows et al. 2011; Zauderer et al. 2011). The Lorentz factor of the jet is highly uncertain, with estimates varying from \( \Gamma \approx 2–5 \) (Zauderer et al. 2011) to \( \Gamma \approx 10 \) (Bloom et al. 2011b; Burrows et al. 2011). The rarity of the event, with one such outburst discovered in 7 years of Swift operations, is consistent with the theoretical expectations of tidal disruption rates and jet opening angle \( \theta \approx 5^\circ \), corresponding to \( \Gamma \approx 1/\theta \approx 10 \).

The origin of the photon emission is still unclear. There are clearly at least two prominent peaks in the spectral energy distribution: one in the far-infrared (far-IR) and the other in the hard X-ray band (Bloom et al. 2011b; Burrows et al. 2011). They can be modelled as direct synchrotron emission (single-component model) from radio to X-rays, with strong dust extinction in the optical/ultraviolet (UV) band. Alternatively, the radio/IR peak is the direct synchrotron emission and the X-ray peak is due to inverse Compton scattering of external photons, most likely disc photons (two-component blazar model). A third possibility is that the X-ray emission is due to inverse Compton emission at the base of the jet, while the radio/IR synchrotron emission comes from the forward shock at the interface between the head of the jet and the interstellar medium (Bloom et al. 2011b).

The X-ray spectrum is well fitted by a simple absorbed power law, although more complex models were also discussed (Burrows et al. 2011). The average photon index during the first \( \approx 2 \times 10^5 \) s is \( \Gamma \approx 1.8 \) (Burrows et al. 2011; Levan et al. 2011a). However, the physical meaning of this average value has to be interpreted more carefully, as there are strong variations in hardness and photon index between flares, with \( \Gamma \) changing between \( \approx 1.3 \) and 3 (Levan et al. 2011a). In particular, the photon index is harder when the source is brighter (Bloom et al. 2011a; Burrows et al. 2011; Kennea et al. 2011; Levan et al. 2011a).

In the Swift X-Ray Telescope (XRT; Burrows et al. 2005) band, 0.3–10 keV, the decline in flux was initially consistent with the \( \Gamma^{-5/3} \) decay (Bloom et al. 2011b; Levan et al. 2011a) expected for the spreading and accretion of fallback material after a tidal disruption event. Bloom et al. (2011b) used the early Swift/XRT observations (up to \( t \approx 4.5 \times 10^5 \) s) to study the power spectral density over the 0.1–100 MHz frequency range: they found no significant feature that is not associated with the orbital period of the spacecraft. In contrast, a series of XMM–Newton Target-of-Opportunity observations during the initial decline phase suggested the presence of a 4.7 MHz (\( \approx 200 \) s) quasi-periodic oscillation (Miller & Strohmayer 2011) and showed short-term variability over the 0.4–100 MHz range. If the putative quasi-periodic oscillation corresponds to the Keplerian frequency at the innermost stable circular orbit of a Schwarzschild BH, it would imply a BH mass of \( \approx 5 \times 10^5 \, M_\odot \) (Miller & Strohmayer 2011).

Possible variability on the \( 10^{-7}–10^{-4} \) Hz frequency range has not been investigated in much detail yet. The ongoing series of Swift/XRT monitoring observations, which have now followed the source for \( \approx 2 \times 10^5 \) s, offer the best chance for this study. Luckily, one year after the outburst, the source is still detected at a flux of \( \approx 10^{-11} \, \text{erg} \, \text{cm}^{-2} \, \text{s}^{-1} \) in the 0.3–10 keV band, declining only very slowly. In this paper, we examine the X-ray variability over the \( 10^7–10^8 \) s time-scale, looking for phenomenological patterns (characteristic variability time-scales and spectral evolution) that can help us test physical scenarios. In particular, we want to determine whether the dips that characterize the X-ray light curve are random or have some periodicity, and we discuss the X-ray changes during the dips.

### 2 DATA ANALYSIS

Sw J1644+57 has been monitored by the XRT several times a day, every day since 2011 March 28. We used the online Swift/XRT data product generator\(^2\) (Evans et al. 2007, 2009) to extract light curves in different energy bands, and spectra (including background and ancillary response files) in different time intervals; we selected grade 0–12 events. We downloaded the suitable spectral response files for single and double events in photon-counting (PC) mode and window-timing (WT) mode from the latest Calibration Database. We used xspec version 12 (Arnaud 1996) for spectral analysis, and standard ftools\(^3\) (Blackburn 1995) tasks for preliminary timing analysis – for example, for defining the time intervals that were used to extract intensity-selected spectra. For more advanced timing analyses, we used a Lomb–Scargle periodogram and structure function analysis (discussed in Section 3 and Appendix A).

A caveat for timing analysis is that the observational data are irregularly sampled; the duration of each snapshot observation in either WT or PC mode (typically, a few hundred seconds) and the temporal gaps between observations are not constant. Irregular, gappy data sequences are accommodated within the formulation of Lomb–Scargle periodograms (Section 3.2.2), where data are at discrete events rather than long temporal bins. Such imperfections however are unnatural to conventional Fourier (Section 3.2.1) and structure function methods (Section 3.2.3). There are various strategies that can circumvent this issue: we considered the hyphen method, the zigzag method and the trapezoid method. In the hyphen method, the gaps are practically omitted. The flux levels are set to be locally constant for the durations of the data bins. In the zigzag method, a data point is set at the mid-time of each observational bin, and we connect each point linearly to the next consecutive data point. The numerical light curve is piecewise linear and resembles a polygonal landscape. In a variant trapezoid method, the observational bins are treated as piecewise flat segments as in the hyphen method but the gaps are connected directly with diagonal lines.

As the covering factor of the bins is small in the hyphen method, unless the data are numerically bridged, we found that the calculated power spectra and structure functions tend to blur any useful information in the noise. Instead, we found that the zigzag method tends

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\(^1\) It has been argued that there may be a second object discovered by Swift in this class (Cenko et al. 2011), and another one discovered by XMM–Newton (Lin et al. 2011).

\(^2\) Including the new treatment of the vignetting correction, introduced after 2011 August 5.

\(^3\) [http://heasarc.gsfc.nasa.gov/ftools](http://heasarc.gsfc.nasa.gov/ftools)
to provide robust results for power spectra and structure functions. The results obtained with the trapezoid method are indistinguishable from those of the zigzag method. Thus, we present here only the results from analyses done with the zigzag method.

3 MAIN RESULTS

3.1 Different phases in the light curve

Fig. 1 shows the XRT 0.3–10 keV light curve, binned by snapshot (typical exposure duration ~ a few 100 s). The luminosity evolution shows a series of phases with different phenomenological properties. During the first three months after the outburst – in particular, at times $2 \times 10^5 \lesssim t \lesssim 9 \times 10^6$ s – the baseline trend is adequately fitted by an exponential decay, with an e-folding time-scale of $\approx 2.0 \times 10^6$ s. Flares and complex dips are superposed on to this trend. In other work (Levan et al. 2011a), a more canonical tidal-disruption decline scaling $\sim t^{-5/3}$ was fitted to the same section of the light curve; the difference is mostly due to a different definition of the baseline. Later, we will show a change in the variability at $t \approx 4.7 \times 10^6$ s, which distinguishes ‘early’ and ‘late’ epochs of the declining stage. For $t \gtrsim 9 \times 10^6$ s, the decay stopped and the source appeared to settle on a ‘plateau’ (XRT count rate $\approx 0.1$ count s$^{-1}$), without any dips. Broader dips resumed for $t \gtrsim 1.25 \times 10^8$ s (the ‘recent’ epoch), but the baseline level has not significantly declined below $\approx 0.1$ count s$^{-1}$.

Because of the different behaviour of the light curve at different epochs, we shall investigate the short-term variability separately in the different phases. We also note that the state transitions are each a continuous, gradual evolution of flux, timing and spectral properties over time. Therefore, the choice of start and end times defining the different epoch sub-intervals is somewhat arbitrary (to within a few $10^5$ s) and does not affect the main conclusions of our study.

3.2 Search for periodicities

3.2.1 Fourier analysis

Fourier techniques, as implemented for example in the XRONOS powspec timing analysis task (Stella & Angelini 1992), are widely used for the timing analysis of X-ray light curves in AGN and X-ray binaries. The standard technique of dividing the light curve into multiple intervals, calculating the power density spectrum in each interval and taking the mean of the power density values (and corresponding standard deviations) is applicable only if the process is ergodic (Priestley 1988; Guidorzi 2011), so that time averages can be substituted for ensemble averages. In the case of highly non-stationary events like Sw J1644+57, gamma-ray bursts, or X-ray flares, it does not make sense to subdivide the light curve into sub-intervals, and the power density spectrum has to be calculated over the entire duration of the observation (Guidorzi 2011). We did that, and then calculated the standard deviation for the power density at each frequency bin with the procedure outlined in Guidorzi (2011).

Fig. 2 shows the power spectrum of the 0.3–10 keV light curve, excluding the first $2 \times 10^5$ s (that is, after the huge initial flares have subsided). The root-mean-square (rms) power rises at lower frequencies, as $\sim \nu^{-1}$. This is mostly due to the long-term dimming trend. There appear to be two unresolved features at frequencies $\nu \approx (2.3 \pm 0.3) \times 10^{-1}$ Hz.
There are plausible periodicities: significant at the 1 per cent FAP level (with two definitions of this threshold marked as horizontal lines).

\[ \approx 2.2 \text{ and } 4.5 \, \mu \text{Hz}; \]

however, their power is comparable to the statistical uncertainty. This prevents us from firmly concluding whether there are true underlying periodicities or whether those features were just statistical noise. Moreover, Fourier analysis techniques are better suited to time series that are equispaced and with no time gaps. Neither condition is true in our case. The complex shape of the window and sampling functions may introduce side lobes (spectral leakage) in the discrete Fourier transform. In summary, we consider the features observed in the power density spectrum as suggestive of possible periodic signals, but not yet statistically significant, because of the shortcomings of the Fourier technique.

### 3.2.2 Lomb–Scargle periodogram

As an improvement over Fourier power spectrum analyses, Lomb (1976) and Scargle (1982) introduced a periodogram technique that proves to be more robust in the detection of periodicities in irregularly sampled light curves. Press & Rybicki (1989) accelerated the method, with a numerical modification based on fast Fourier transforms. The Lomb–Scargle periodogram is equivalent to a best-fitting analysis of the data with a single sinusoidal function. The phase and amplitude emerge directly for the implied fit. The technique is observationally applied to diverse subjects: exoplanet detections, solar eruptions, variable and pulsating stars, high-energy accreting systems and ultracompact binaries (e.g. Hakala et al. 2003; Wen et al. 2006; Foullon, Verwichte & Nakariakov 2009; Sarty et al. 2009; Farrell et al. 2010; Nataf, Stanek & Bakos 2010; Qian, Solomon & Mlynczak 2010; Desidera et al. 2011; Ness et al. 2011; Omiya et al. 2012; Uthas et al. 2012; Xu et al. 2011).

Fig. 3 presents Lomb–Scargle plots of four stages of the light curve: during the early decline \((4 \times 10^5 < t < 4.7 \times 10^6 \text{s})\), late decline \((4.7 \times 10^6 < t < 9 \times 10^6 \text{s})\), the plateau \((9 \times 10^6 < t < 1.25 \times 10^7 \text{s})\) and the recent post-plateau stage \((t > 1.25 \times 10^7 \text{s})\).

We used a freely available IDL code\(^4\) implementing the formulation of Press & Rybicki (1989) and Horne & Baliunas (1986). Power and detection thresholds assume a grid of 1000 evenly spaced frequencies. For the sake of smoother curves, the curve is drawn with \(10^4\) intermediate frequencies (not involved in the calculation of detection thresholds). In our plots, peak detection thresholds are marked in blue and red. Higher peaks are statistically significant at the 1 per cent level (‘false alert probability’, FAP = 0.01). The blue (dashed) threshold is \(z_0\) in equation (18) of section III(c) of Scargle (1982).

The red (dot–dashed) line is the threshold obtained from \(10^5\) ‘white noise simulations’ conservatively taking the light curve’s total variance. The data are not de-trended, so the variance is an overestimate. The uncorrected decay time-scale \((t_0 \approx 2 \times 10^6 \text{s})\) during the early and later decline \((t < 9 \times 10^6 \text{s})\) is probably responsible for artefacts at the long-period end of the periodograms (top panels of Fig. 3).

At early times \((t < 4.7 \times 10^6 \text{s})\) there are peaks of varied significance at periods of \(\tau \approx 0.23, 0.45, 0.9\) and 1.4 Ms. The first two in this series correspond to the two features tentatively identified in the Fourier spectrum (Section 3.2.1). A characteristic spacing

\[^4\] http://astro.uni-tuebingen.de/software/idl/aitlib/timing/
of $\approx 0.45$ Ms between dips is also inferred from a visual inspection of the early part of the XRT light curve (Fig. 4). During later weeks of the decline ($4.7 \times 10^5 < t < 9 \times 10^5$ s) there is a stronger peak at period $\tau \approx 0.9$ Ms. Later, during the plateau stage ($9 \times 10^5 < t \lesssim 12.5 \times 10^5$ s), the power of the peaks is relatively low, consistent with the visible steadiness of the light curve. There may be a feature at $\tau \approx 1.1 \times 10^5$ s, which is near the 1 per cent significance level, and perhaps another, weaker, feature at $\approx 0.4 \times 10^5$ s. In the very latest times after the plateau, when dipping resumed ($t \gtrsim 12.5 \times 10^5$ s), there is a strong peak at $\tau \approx 1.4$ Ms. This is consistent with a visual inspection of the last section of the light curve, as it is the characteristic spacing between major quasi-sinusoidal dips (Fig. 4).

In summary, the Lomb–Scargle analysis gives signs of periodicity (which are stronger in some intervals than others), and these indications are clearer than those from the Fourier analysis. We note that the Lomb–Scargle periodogram is by construction most sensitive to oscillations similar to a sine wave. Repetitive patterns that are highly non-sinusoidal may have their true significance understated. The dips seen in the early phases of the XRT light curve (Fig. 4) are sharp and brief compared to the non-dip conditions: this is clearly far from a sinusoidal pattern. This motivates further study with another, broader technique.

### 3.2.3 Structure function technique

To obtain a more robust test of the presence or absence of periodicity in the X-ray luminosity variations, we carried out a more effective alternative analysis based on Kolmogorov’s structure functions (Kolmogorov 1941, 1991). They are the statistical moments of a temporally varying signal, with the light curve compared to itself at an offset $\tau$. The nth-order structure function is

$$S_n(\tau) \equiv \langle [z(t + \tau) - z(t)]^n \rangle.$$  

The second-order structure function, $S_2$, is particularly useful for the purpose of time-series analysis, as it describes the variance of a signal on time-scales $\tau$. In addition to their original applications in the physics of turbulence (Brandenburg & Nordlund 2011 and references therein), structure functions have a venerable history in the diagnosis of variability in blazars, other configurations of AGN and various compact systems (e.g. Cordes & Downs 1985; Simonetti, Cordes & Heeschen 1985; Bregman et al. 1988; Hughes, Aller & Aller 1992; Brinkmann et al. 2000, 2001; Iyomoto & Makishima 2001; Kataoka et al. 2001; Tamihata et al. 2003; Willhite et al. 2008; Emmanoulopoulos, McHardy & Uttley 2010; Voevodkin 2011; Yusef-Zadeh et al. 2011). In these contexts, they are most often used to search for break frequencies that are supposed to characterize internal scales of the system, though Emmanoulopoulos et al. (2010) warn users to beware of potential artefacts from sparsely sampled data. (Our data are densely sampled, even during the dips, and we are seeking signs of repetition rather than break scales.) Structure functions are also used to diagnose simulations of turbulence in interstellar media (Boldyrev, Nordlund & Padoan 2002; Kritsuk et al. 2007; Schmidt, Federrath & Klessen 2008; Kritsuk et al. 2009), and synthetic observables of simulated jets and AGN (Saxton et al. 2002, 2010). In Appendix A, we show the procedures by which we compute the structure functions of various orders from data sets with unevenly sampled data. We also show how the corresponding uncertainties are determined. In the rest of this section, we report our main findings.

As the X-ray light curve is not a simple exponential or power-law decline, but seems to go through phases of different slope, we calculated separate structure functions during different time intervals, to determine whether the characteristic variability time-scale changed in different epochs. We calculated two sets of functions: one with the count rates directly detected by the XRT; the other with a de-trended count rate, to remove the long-term evolution (time-scale of weeks/months) and highlight the short-term variability (time-scale of a few days). At early epochs (in particular, at times $2.0 \times 10^5 \lesssim t \lesssim 9.0 \times 10^5$ s; Fig. 1), multiplying the count rate by an exponential function $\exp (t/t_0)$, with $t_0 \approx 2.0 \times 10^5$ s, is a simple way to correct for the long-term evolution. For the whole light curve (including the later plateau stage), a simple exponential or power-law function is not applicable; we used empirically fitted rational functions. Note that the results that we obtained are independent of the precise choice of normalizing function for the count rate, and including or omitting data from the first few days also does not significantly alter the outcome. Our choice of binning (for example, using the same binning of the snapshot observations, or a fixed time binning of 100 or 200 s) does not have significant effects either.
Table 1. Time-scale of regular features detected in the $S_\nu(\tau)$ structure function for data extracted in the intervals $\Delta t_1 = [0.4, 8.9] \times 10^6$ s and $\Delta t_2 = [1.0, 8.9] \times 10^6$ s. Minima are tabulated if their depths exceed $1 \sigma$ and $3 \sigma$ locally, and are not enclosed within the catchment of another local minimum. To emphasize the periodicity, we express the time-scales $\tau$ as multiples of a characteristic $\tau_0 = 0.445 \times 10^6$ s.

| $\Delta t_1$, $1\sigma$ | $\Delta t_1$, $3\sigma$ | $\tau/\tau_0$ | $\Delta t_2$, $1\sigma$ | $\Delta t_2$, $3\sigma$ |
|------------------------|------------------------|----------------|------------------------|------------------------|
| 0.514$^{+0.014}_{-0.038}$ | 0.514$^{+0.031}_{-0.074}$ | 0.478$^{+0.017}_{-0.037}$ | 0.478$^{+0.003}_{-0.039}$ | 0.445 |
| 1.037$^{+0.014}_{-0.024}$ | 1.037$^{+0.035}_{-0.043}$ | 1.060$^{+0.017}_{-0.027}$ | 1.060$^{+0.040}_{-0.053}$ | 0.445 |
| 1.555$^{+0.016}_{-0.026}$ | 1.555$^{+0.031}_{-0.046}$ | 1.501$^{+0.024}_{-0.020}$ | 1.501$^{+0.059}_{-0.034}$ | 0.445 |
| 2.034$^{+0.036}_{-0.054}$ | 2.034$^{+0.036}_{-0.058}$ | 1.994$^{+0.031}_{-0.020}$ | 1.994$^{+0.053}_{-0.038}$ | 0.445 |
| 2.455$^{+0.034}_{-0.052}$ | 2.455$^{+0.076}_{-0.095}$ | 2.464$^{+0.061}_{-0.034}$ | 2.464$^{+0.082}_{-0.056}$ | 0.445 |
| 3.052$^{+0.033}_{-0.052}$ | 3.052$^{+0.057}_{-0.095}$ | 3.048$^{+0.048}_{-0.038}$ | 3.048$^{+0.076}_{-0.088}$ | 0.445 |
| 3.558$^{+0.027}_{-0.043}$ | 3.558$^{+0.048}_{-0.062}$ | 3.585$^{+0.025}_{-0.052}$ | 3.585$^{+0.053}_{-0.092}$ | 0.445 |
| 4.002$^{+0.045}_{-0.064}$ | 4.002$^{+0.084}_{-0.110}$ | 4.024$^{+0.025}_{-0.064}$ | 4.024$^{+0.065}_{-0.103}$ | 0.445 |
| 4.498$^{+0.048}_{-0.064}$ | 4.498$^{+0.068}_{-0.100}$ | 4.464$^{+0.058}_{-0.058}$ | 4.464$^{+0.089}_{-0.152}$ | 0.445 |
| 5.066$^{+0.064}_{-0.097}$ | 5.066$^{+0.110}_{-0.125}$ | 4.976$^{+0.057}_{-0.027}$ | 4.976$^{+0.178}_{-0.097}$ | 0.445 |
| 5.536$^{+0.095}_{-0.138}$ | 5.536$^{+0.139}_{-0.245}$ | 6.139$^{+0.068}_{-0.112}$ | 6.139$^{+0.122}_{-0.173}$ | 0.445 |
| 6.036$^{+0.074}_{-0.101}$ | 6.036$^{+0.112}_{-0.185}$ | 7.629$^{+0.068}_{-0.139}$ | 7.629$^{+0.122}_{-0.208}$ | 0.445 |
| 8.531$^{+0.108}_{-0.100}$ | 8.531$^{+0.112}_{-0.100}$ | 8.531$^{+0.122}_{-0.122}$ | 8.531$^{+0.122}_{-0.122}$ | 0.445 |

What we are looking for in a structure function $S_\nu(\tau)$ are local depressions around specific $\tau$ values: they indicate that the light curve is repetitive on that period. We obtain best estimates of the periods by numerically locating the minima in $S_\nu$ (the smoothest structure function) and then discarding all those that are shallower than the local uncertainty $1\sigma$ ($1\sigma$ result) or $3\sigma$ ($3\sigma$ result). We discard the lesser minima that are within the $1\sigma$ ($3\sigma$) catchments of wider and deeper minima. Table 1 shows results obtained from data spanning the decaying phase of the light curve.

3.2.4 Variability during the decay phase

The most significant result of our analysis is that for $t \lesssim 9 \times 10^6$ s, all structure functions exhibit strong minima at integer and half-integer multiples of a basic period $\tau \approx 4.5 \times 10^6$ s (see Fig. 5 for the very early epoch and Fig. 6 for a later epoch). Most of these features are many times deeper than the sizes of the statistical uncertainties. Corresponding features appear in structure functions of different order. There is also a significant difference between structure functions calculated for early epochs ($t \lesssim 4.7 \times 10^6$ s) and later in the decline phase ($4.7 \times 10^6 \lesssim t \lesssim 9.0 \times 10^6$ s). At early epochs, the most prominent feature is in fact at $\tau \approx 2.3 \times 10^6$ s, that is half of what we identified as some kind of fundamental time-scale. Fig. 5 shows 17 consecutive features in the structure functions, at integer multiples of $2.3 \times 10^6$ s. At later times, the shorter periods ($\tau \approx 2.3 \times 10^6$ s and $\tau \approx 4.5 \times 10^5$ s) fade and remain only marginally detectable in the higher order structure functions. Instead, the deepest features in the structure functions are at $\tau \approx (0.9, 1.8, 2.7, 3.6) \times 10^6$ s, higher multiples of the fundamental time-scale (Fig. 6).

The characteristic time-scales found from structure function analysis (in particular, the features at $2.3 \times 10^6$, $4.5 \times 10^5$ and $9 \times 10^5$ s) confirm and strengthen the results obtained from the Lomb–Scargle periodogram (Section 3.2.2) and are consistent with a visual inspection of the light curve (Fig. 4). The two shortest frequencies also correspond to the two features we identified as marginally significant in the power density spectrum (Section 3.2.1). None of these time-scales appear to be exact periodicities: sometimes a major dip may commence slightly earlier or later than this time interval, or
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3.2.5 Variability during the plateau phase

After $t \approx 9 \times 10^6$ s, the slope of the long-term trend flattened and the light curve settled on a plateau (Fig. 1), with an X-ray count rate $\approx 0.1$ count s$^{-1}$. At the same time, major dips, which had punctuated the light curve until then, appeared to vanish. Structure functions calculated for the plateau stage do not show any significant periodicity (Fig. 7). Depending on the specific choice of de-trending function, the fluctuations are ‘white noise’ (flat shape) or flattish ‘red noise’ (rising at long $\tau$) for time-scales $\tau \gtrsim 5 \times 10^4$ s. As always, at shorter time-scales the slopes of the structure functions indicate red noise down to the orbital period of Swift and the typical gap interval between observations.

3.2.6 Variability during later epochs

A dipping behaviour began again at $t \approx 1.25 \times 10^7$ s. The range of count rate variability is about the same as in the early phases, that is a factor of $\approx 10$–20 between peaks and troughs, but the dips are broader. The dip duration has become comparable to the orbital period of Swift and the typical gap interval between observations.

duration. In the early epochs, the typical duration of a dip is $\sim 1$ d; at later epochs, it is $\sim 10$ d (cf. top and bottom panels of Fig. 4).

Fig. 8 shows the structure functions of the de-trended light curve during the most recent epoch. There are minor wiggles at 0.1 Ms time-scales. These are probably spurious, as they are comparable to the gaps between observations. When the whole time interval $t \gtrsim 1.25 \times 10^7$ s is included in the structure function calculation (top panel of Fig. 8), it is not immediately obvious whether there are dominant time-scales. This is partly because the Swift monitoring observations have become less frequent, and partly because the source has not varied much after $t \approx 1.85 \times 10^7$ s. Taking only the sub-interval $1.25 \times 10^7 < t < 1.85 \times 10^7$ s, when the source is more variable, reveals clearer features at $\tau \approx 0.7$, 1.4, 2.9, 4.3, 5.0 and 5.7 Ms (bottom panel of Fig. 8) – all simple multiples of the same basic frequency, although it is a different base frequency than the one associated with the narrow dips in the initial rapidly declining stages. The variability time-scale $\tau \approx 1.4 \times 10^6$ s was also identified at high significance in the Lomb–Scargle periodograms (fourth panel of Fig. 3). In fact, it appears more significant in the Lomb–Scargle periodograms than in the structure functions. This is probably because of the nearly sinusoidal waveform of the recent oscillations.

3.3 Time-dependent spectral properties

3.3.1 Hardness ratio evolution

It was noted in previous work (Burrows et al. 2011; Levan et al. 2011a) that the X-ray emission of Sw J1644+57 is harder (flatter spectrum) when the source is brighter. However, this one-dimensional correlation cannot fully characterize the spectral
behaviour. The count rate drops during the short-term dips, but also as a result of the long-term evolution: we need to treat the two effects separately, as they probably have different physical origins. To do so, we divided the light curve into several time intervals, similar to our approach with the Lomb–Scargle periodograms and structure function analysis; the intervals are also defined in approximately the same way for convenience, although the precise start and end of each phase is somewhat arbitrary. We plotted the hardness ratio (defined as the observed count rate in the 1.5–10 keV band over that in the 0.3–1.5 keV band) as a function of total count rate for each segment, in different colours, in Fig. 9.

At early times, the general trend is a moderate hardening as the baseline flux declines, alternating with significant softening during each dipping episode. This is particularly evident in the distribution of data points coded with red, green and magenta colours in the top two panels of Fig. 9, which cover the time interval $2 \times 10^5 < t < 4.7 \times 10^6$ s. Further independent confirmation of the softening behaviour during the dips comes from XMM–Newton observations taken on 2011 April 16, April 30, May 16 and May 30. The power-law photon indices measured during the first, second and fourth observations were $\Gamma_1 \approx 1.88, 1.66$ and $1.61$, respectively (Miller & Strohmayer 2011), consistent with the moderate long-term hardening as the baseline flux declined; but the third observation occurred during a dip, and the photon index was $\Gamma_1 \approx 1.97$.

At later times, as the light curve reaches a plateau and dips become less frequent, the hardness ratio also seems to settle around a constant value corresponding to $\Gamma_1 \approx 1.4$, with some scatter mostly

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**Figure 8.** Structure functions of the de-trended X-ray light curve, for the recent epoch following the end of the plateau stage. The top panel is integrated over the whole available sequence ($t > 1.25 \times 10^7$ s). The bottom panel uses only a shorter interval ($1.25 \times 10^7 < t < 18.5 \times 10^7$ s) before the observations became too sparse.

**Figure 9.** Top panel: hardness–intensity diagram for the snapshot data points in PC mode. Red data points are those for $t < 1.25 \times 10^6$ s, green data points for $3.41 \times 10^6 < t < 4.7 \times 10^6$ s, blue data points for $4.7 \times 10^6 < t < 9 \times 10^6$ s and orange data points for $9 \times 10^6 < t < 1.25 \times 10^7$ s. Error bars have been omitted for clarity. The horizontal dashed lines correspond to the hardness ratio expected in PC mode for a power-law spectrum with intrinsic column density $N_H = 1.5 \times 10^{22}$ cm$^{-2}$ (at redshift 0.354), a Galactic absorption $N_H = 2 \times 10^{20}$ cm$^{-2}$ and several different values of the photon index $\Gamma$. Middle panel: hardness–intensity diagram for the data points in WT model, at time $1.25 \times 10^6 < t < 3.41 \times 10^6$ s, with intrinsic $N_H = 1.5 \times 10^{22}$ cm$^{-2}$. Bottom panel: hardness–intensity diagram in PC mode for the last part of the light curve ($1.25 \times 10^7 < t < 2.1 \times 10^7$ s), binned to observation data points; an intrinsic $N_H = 1.9 \times 10^{22}$ cm$^{-2}$ was used for this late epoch, as suggested by our spectral fitting (see Section 3.3.2).
due to the small number of counts in each snapshot observation. When the dipping behaviour resumes, at time \( t \approx 1.25 \times 10^7 \) s, the hardness ratio no longer changes during the dips (bottom panel of Fig. 9), in contrast with the behaviour at early times.

In summary, we found that at early epochs, the dips are shorter, sharper and significantly softer than the baseline emission at the same epoch. At late times, instead, the dips become broader and longer, and the hardness ratio is independent of flux. We sketch our interpretation of the flux-hardness evolution in Fig. 10.

### 3.3.2 Spectral evolution

Our investigation of hardness evolution makes it clear that we need to distinguish between the short-term and long-term spectral evolution. To do so, we use the same method as applied to our function analysis: we normalized the snapshot light curve to a smooth empirical function that fits the long-term evolution. We then extracted intensity-selected spectra based on the normalized count rates rather than the observed ones; for example, integrated spectra from all time intervals in which the normalized flux was \( >0.9 \), or between 2/3 and 0.9, etc. We also fixed the flux level and extracted time-selected spectra, that is with the same normalized flux band but at different epochs.

In Table 2, we summarize the result of spectral fitting for a sample of intensity-selected spectra from the decline phase (\( t < 9 \times 10^6 \) s).

All spectra are well fitted by absorbed power laws, with a column density of \( \sim 1.5 \times 10^{23} \) cm\(^{-2} \) in the local frame at redshift 0.354. Small variations in the fitted column density from band to band may not be statistically significant, and do not appear to follow any trend. The high- and medium-intensity bands have a similar photon index \( \approx 1.7 \). Low-intensity bands have a steeper slope, as already suggested by our hardness ratio analysis: as steep as \( \Gamma \approx 2.9 \) for spectra taken across the bottom of the dips (Fig. 11). This result confirms our interpretation of the hardness–intensity plots and is consistent with the spectral results of Miller & Strohmayer (2011). It shows even more clearly that the early dips are characterized by a steeper spectral slope, not by higher absorption: they are not eclipses by orbiting or rotating clouds.

We then considered high- and medium-intensity spectra (which, as we have seen from Table 2, have the same average spectral slope), from all time intervals with normalized count rates \( >2/3 \), and divided them into several time bands corresponding to the intervals used for timing analysis. We found (Table 3) that all spectra are well fitted by a simple absorbed power law; adding blackbody or optically thin thermal components does not improve the fit, nor is there any evidence of breaks in the power law at high energies. The slope in the early epoch (\( t < 4.7 \times 10^6 \) s) was \( \Gamma \approx 1.8 \), flattening to \( \Gamma \approx 1.4–1.5 \) at later epochs (Fig. 12). This long-term spectral trend is in perfect agreement with what was inferred from the hardness–intensity study (Section 3.3.1 and Fig. 10). The intrinsic column density appears to increase at later epochs (Table 3), although this result is only marginally significant.

At late epochs, the unabsorbed isotropic 0.3–10 keV luminosity becomes as low as \( \sim 4 \times 10^{36} \) erg s\(^{-1} \) during the dips (Table 4). This is now approaching the pre-burst upper limit to the X-ray

| Parameter | Band 1 value | Band 2 value | Band 3 value | Band 4 value | Band 5 value |
|-----------|--------------|--------------|--------------|--------------|--------------|
| \( N_{H, \text{Gd}} \) | 0.190.02 | 0.2 | 0.02 | 0.02 | 0.02 |
| \( N_{H, \text{Gd}=0.354} \) | 1.010.012 | 1.010.09 | 1.210.12 | 1.140.12 | 1.140.12 |
| \( \Gamma \) | 1.770.08 | 1.720.08 | 1.680.04 | 1.820.09 | 2.870.47 |
| \( N_0 \) | 14.610.2 | 12.010.9 | 8.210.4 | 3.510.4 | 1.810.6 |
| \( f_{0.3–10} \) | 7.710.1 | 5.310.1 | 3.810.1 | 1.310.1 | 0.2010.02 |
| \( L_{0.3–10} \) | 46.810.6 | 32.410.4 | 22.510.6 | 8.910.5 | 5.810.8 |
| \( \chi^2 \) | 1.06 | 0.96 | 0.96 | 0.98 | 1.03 |
| (328.3/311) | (271.1/282) | (461.1/480) | (155.2/158) | (26.8/26) |
luminosity, $L_X \lesssim 1.7 \times 10^{34}$ erg s$^{-1}$ (Bloom et al. 2011b). If Sw J1644+57 continues its decline, it is plausible that in a few months’ time we will start seeing the unbeamed component of the emission (e.g. from an accretion disc or its corona), or we will infer stronger limits on the unbeamed flux. We tried fitting the late-epoch dip spectrum with a thermal-plasma model and found that it is at least as good as a power-law model (Table 4); there are not enough counts to discriminate between them.

4 DISCUSSION

The general consensus is that Sw J1644+57 is a previously quiescent nuclear BH that underwent an outburst caused by accretion of a tidally disrupted star (Bloom et al. 2011a,b; Burrows et al. 2011; Cannizzo et al. 2011; Socrates 2012). Its high apparent luminosity requires strong beaming. The emission in the keV band can be explained as synchrotron and/or inverse Compton radiation from energetic electrons streaming along the relativistic jet pointing towards us. The relative contribution of the two processes is still debated. It is also still unclear how the jets are launched at the onset of the outburst, when a fully formed accretion disc cannot have had the time to develop, after the disruption event (cf. the violent mass transfer and jet formation in the X-ray binary Cir X-1; Johnston, Fender & Wu 1999).

Table 3. Best-fitting spectral parameters for time-selected Swift/XRT-PC spectra. All spectra include only intervals in which the count rate was $>2$ of the normalized continuum rate. Band A is for time intervals $2 \times 10^5 < t < 4.7 \times 10^5$ s; band B is for $4.7 \times 10^5 < t < 9 \times 10^5$ s; band C is for $9 \times 10^5 < t < 1.25 \times 10^6$ s; and band D is for $1.25 \times 10^6 < t < 2.1 \times 10^6$ s. Units are as in Table 2. Errors indicate the 90 per cent confidence interval for each parameter of interest.

| Parameter | Band A value | Band B value | Band C value | Band D value |
|-----------|--------------|--------------|--------------|--------------|
| $N_{\text{H(Gd)}}$ | [0.02] | [0.02] | [0.02] | [0.02] |
| $N_{\text{H(z)}}$ | 1.50$^{+0.07}_{-0.09}$ | 1.54$^{+0.19}_{-0.20}$ | 1.79$^{+0.06}_{-0.09}$ | 1.92$^{+0.39}_{-0.34}$ |
| $\Gamma$ | 1.77$^{+0.05}_{-0.11}$ | 1.41$^{+0.03}_{-0.11}$ | 1.46$^{+0.04}_{-0.04}$ | 1.50$^{+0.18}_{-0.17}$ |
| $N_{\text{po}}$ | 30.2$^{+1.8}_{-1.6}$ | 1.6$^{+0.03}_{-0.2}$ | 1.3$^{+0.1}_{-0.1}$ | 1.0$^{+0.3}_{-0.2}$ |
| $f_{0.3-10}$ | 12.2$^{+0.1}_{-0.2}$ | 11.1$^{+0.1}_{-0.1}$ | 0.91$^{+0.05}_{-0.06}$ | 0.54$^{+0.05}_{-0.07}$ |
| $L_{0.3-10}$ | 80.8$^{+2.9}_{-1.7}$ | 5.7$^{+0.3}_{-0.3}$ | 4.5$^{+0.1}_{-0.1}$ | 3.7$^{+0.2}_{-0.2}$ |
| $\chi^2$ | 1.06 | 0.99 | 0.92 | 1.06 |
| (432/3408) | (95.6/106) | (487.5/528) | (78.4/74) |

Table 4. Best-fitting spectral parameters for the Swift/XRT-PC spectrum during the late dips (1.25 $< t < 2.1 \times 10^6$ s), fitted with the standard power-law model and with an optically thin thermal plasma model. Units of $N_{\text{H}}$, flux and luminosity are as in Table 2. The normalization $N_{\text{H}} = 10^{-11}(1 + z^2)/(4\pi D^2)$, where $D$ is the luminosity distance. Errors indicate the 90 per cent confidence interval for each parameter of interest.

| Parameter | Value 1 | Value 2 |
|-----------|---------|---------|
| $N_{\text{H(Gd)}}$ | [0.02] | [0.02] |
| $N_{\text{H(z)}}$ | 1.8$^{+1.6}_{-1.3}$ | 1.7$^{+1.2}_{-0.9}$ |
| $\Gamma$ | 1.58$^{+0.73}_{-0.70}$ | - |
| $f_{0.3-10}$ | 0.14$^{+0.07}_{-0.07}$ | - |
| $L_{0.3-10}$ | 0.45$^{+0.30}_{-0.10}$ | 0.39$^{+0.08}_{-0.04}$ |
| $C$-stat | 7.35/12 | 6.16/12 |
From the Swift/XRT data we have extracted further information on the time-dependent behaviour and spectral evolution of the source. We have decomposed the amplitude variations into a long-term evolution (an initial decline followed by a plateau) and recurrent dips. If these dips had been wholly stochastic processes, we would expect that fluctuations should be of the same order of magnitude as the depths of the dips. Otherwise it would require many miniature flares (a day’s worth of them) to coherently conspire to become small simultaneously, or to abstain simultaneously.

However, we have shown that the dips are not merely random fluctuations (as is often the case in the X-ray light curve of accreting sources), but have a certain regularity, apparently governed by an underlying periodic driver. We have used Lomb–Scargle periodograms and structure function analysis to search for the main characteristic time-scales in the frequency range $\sim 10^{-7}$–$10^{-4}$ Hz. We expect variability on those time-scales based on physical arguments. For example, there may be a residual inhomogeneous distribution of debris at or near the tidal disruption radius $R_{TD} \approx 10GM/c^2 \times [M_*/(10^7 M_\odot)]^{-2/3}$ (for a solar-type star). The Kepl erian time-scale $t_K = 2\pi/\Omega_1$ at the tidal disruption radius is $\approx 10^3$ s (Rees 1988), independent of BH mass in the Newtonian approximation. The ring of debris is likely to be still oriented in the orbital plane of the disrupted star: this may generate a Lense–Thirring precession with a time-scale of $t_{LT} = [t_K/(2\alpha)] \times [(R_{TD}c^2)/(GM_*)]^{1/2} \sim 30$–$300 t_K/(2\alpha) \sim 10^7$–$10^8$ s (Armitage & Natarajan 1999; Merritt et al. 2010; Stone & Loeb 2012), where $\alpha$ is the BH spin parameter.

We found significant features in the Lomb–Scargle periodograms and structure functions, especially at $\tau \approx 2.3$, 4.5 and 9 Ms during the early epochs, and $\tau \approx 0.7$ and 1.4 Ms during the late epochs. It appears that the characteristic dipping time-scale (and its associated harmonics) has shifted between the early and late sections of the light curve.

Whatever the mechanism for the dips, it is something that also changes the spectral properties of the emission, as the spectrum is steeper during the early dips ($\Gamma \approx 2.8$–3) than immediately before and after ($\Gamma \approx 1.4$–1.7). At the same time, the long-term trend outside the dips shows spectral hardening at the beginning, followed by a plateau at $\Gamma \approx 1.4$.

Here, we attempt to make sense of our findings in the framework of a synchrotron-emitting relativistic jet scenario. We propose that: (i) the jets have precessional and nutational motion; (ii) the jets have a collimated core surrounded by an envelope of less energetic, less collimated electrons straying out of the core; and (iii) the synchrotron-emitting jets become more compact as the source declines, after the initial outburst.

In this scenario, the baseline flux in the XRT band is direct synchrotron emission from a jet pointing towards us. In the first few days after the outburst, when the accretion rate is highest, the jet expands and propagates forward into the interstellar medium. The X-ray emission region is most extended at that early epoch, and it is optically thin to synchrotron radiation. Energetic electrons are freshly accelerated in the jets, with an energy distribution $N(E) \propto E^{-p}$, where the energy spectral index is $2.2 \lesssim p \lesssim 2.5$ (see e.g. Ballard & Heavens 1992; Kirk & Duffy 1999). The synchrotron emission spectrum from this population of electrons has a specific intensity $I_\nu \propto \nu^\alpha$ with $\alpha \approx 0.7$, corresponding to a photon index of $\Gamma \approx 1.7$. When the most violent flarings subside and accretion becomes more steady, the overall accretion luminosity of the system decreases and the jet power is reduced accordingly. In this phase, synchrotron emission no longer comes from the expanding jet ejecta, but it is rather confined to the vicinities of shocks at the base of the jet. As the X-ray emission region becomes more compact and denser, the synchrotron photons start to suffer self-absorption, leading to the observed spectral flattening: approaching a similar situation to the flat-spectrum core emission in radio galaxies with compact jets.

Moreover, the transition from extended to compact jet emission may also provide a simple explanation for the levelling off of the X-ray luminosity at late epochs. For an optically thin source, the luminosity depends on the total volume of the synchrotron-emitting region in the jets; a constant luminosity would require a high degree of fine-tuning. In contrast, in an opaque source, the luminosity depends on the effective area of the emission region visible to us. The growth of the radio-emitting region is perhaps explained by a more diffuse outer region, such as the larger jet-driven turbulent cocoon and the expanding bow shock surrounding the whole system (Bower et al. 2011; Burrows et al. 2011; Zauderer et al. 2011). Modelling the radio flux evolution requires knowledge of the jet parameters, which are unfortunately not well constrained by the observational data obtained so far. We therefore leave the jet modelling, which is beyond the scope of this paper, to a future study.

Regarding the dips, we showed that they are not due to partial occultation of the jets by some line-of-sight material, as we would expect higher absorption rather than spectral steepening in this situation, contrary to what is observed. Instead, we propose that dips occur when the synchrotron-emitting jet is not perfectly aligned along our line of sight, and hence the most highly beamed component of the synchrotron emission does not reach us. The observed X-ray flux is then dominated by the lower level of emission from the slower and/or less collimated electrons in a sheath or cocoon around the jet. This emission could be synchrotron from an aged (steeper spectrum) population of electrons, if there are significant magnetic fields in the jet envelope, or synchrotron self-Compton. We must also stress that even at the bottom of the dips, the apparent luminosity is higher or similar (for the late dips) to the Eddington luminosity of a $10^7$–$M_\odot$ BH. This suggests that the emission is moderately beamed even during the dips.

In addition to the expected long-term decline and stochastic flux variability, it is intriguing that many of the dips occur on regular patterns, likely to be governed by a periodic driver; it is even more intriguing that sometimes a dip is skipped but the following one happens again approximately at the expected phase (Fig. 4). A careful inspection of the centroid locations of the dips has revealed that they are not exactly phase matched but can be slightly advanced or delayed. To explain these peculiar dip patterns, we propose that the jet undergoes nutation as well as precession. The combination of the two effects drives the cone of the jet out of our line of sight, from time to time. The presence of nutation is essential, as it naturally explains why the dips occur in a regular but not exactly periodic pattern, and why there are slight advances or delays of the dip centroids.

We also note that the appearance of the dips changes: in the early epoch we see a slow fading and rapid rise; but in later dips the dimming and rising are symmetric (Fig. 4). The fractional time that the object is in a dip or out of a dip also changes: brief dips at early times, long dips in late epochs. These observations gain significance in the jet precession/nutation scenario, especially if the emission core became more compact. When the early dips were sharp and brief, the precession subtended a tight angle, compared to the jet’s beaming angle. The larger width of the dips at late times and the larger fraction of time spent in a dip probably indicate that the core of the jet is narrower (or swinging more widely) while the layer of slower electrons around the core grows in size. The asymmetric dipping at early times may mean that the region around the core is not moving in phase with the jet core: lagging while the
core moves out of the line of sight, while being compacted when the core moves back.

The remaining question is what causes the jet precession and nutation. Jet precession is expected as the BH spin axis is unlikely to be perfectly aligned with the initial angular momentum of the disrupted star. Thus, the normal direction to the plane of the transient accretion ring/disc formed by the stellar debris is tilted with respect to the BH spin, and this causes the jet to precess. In addition, jet nutation can be triggered if the precessing jet/disc system has been perturbed, either by an internal or external driver. In the internally driven case, nutation may be induced by an uneven mass distribution in the transient debris ring/disc. In the externally driven case, the jet and the accretion ring/disc may be perturbed by the orbiting remnant of the partially disrupted star – for example, a white dwarf on an elliptical orbit would make several passes inside the tidal radius before being completely disrupted (Krolik & Piran 2011). Alternatively, they may be perturbed by another gravitating object, such as (unlikely but not impossible) a satellite massive black hole (as predicted in nuclear swarms of compact objects; Freitag,amaro-Seoane & Kalogera 2006; Portegies Zwart et al. 2006), or perhaps a more supermassive companion (about which Sw J1644+57 is the satellite).

An important clue to the evolution of the system comes from the change in the characteristic variability time-scales at early and late times. If the nutation is externally driven, the change of period might conceivably be explained if the torque changed (perhaps during an eccentric perimelasma passage). Scenarios dominated by disc torques suggest other possibilities. A possible explanation is that the warped disc has not yet reached a steady state or Bardeen–Petterson regime (Bardeen & Petterson 1975; Kumar & Pringle 1985). In other words, the warp radius (transition between the inner part of the disc aligned with the BH spin and the outer part aligned with the orbital plane of the mass donor) may still be propagating outwards, and as a result the Lense–Thirring precession time-scale at the warp radius is increasing. Alternatively, it was suggested (Fragile et al. 2007; Dexter & Fragile 2011; Stone & Loeb 2012) that a geometrically thick disc may never settle in a Bardeen–Petterson regime, and may instead precess as a solid body (a tilted, rather than warped disc). In this case, the precession frequency depends on the dimensionless radial surface density profile of the disc, which is also likely to evolve in time.

In fact, a problem of the disc-driven precessing-jet scenario is that we expect the jet axis to have already precessed out of alignment with our line of sight (and not just for short dips) after few weeks, unless the initial alignment of the disc and BH spin axis was already very close (Stone & Loeb 2012). This seems an unlikely coincidence if the disc was formed after a tidal disruption event. Thus, we suggest a note of caution regarding the tidal disruption scenario as the origin of the flare. It is useful to remember that the 2011 March 28 flare marks the moment when the jet turned on, not the time of the putative tidal disruption event, which may have happened unobserved several weeks earlier, depending on the time required to spread the debris on to a disc, build up a magnetic field and launch a jet. The main argument for a tidal disruption as the origin of the whole process is that the host galaxy was not known as an AGN before the flare. However, pre-event luminosity upper limits (Bloom et al. 2011b) are only implying that the bolometric luminosity was below Eddington for a $10^{-5}$M$_\odot$ BH, or below 10 Eddington for a $10^5$M$_\odot$ BH. Thus, we cannot expect that an accretion disc was already present and approximately aligned, and the jet ejection was due to a state transition rather than a tidal disruption. State transitions with relativistic blob ejections and radio/X-ray flares are common in Galactic BH transients, especially when they switch from the hard to the soft (thermal) state (Fender & Belloni 2004; Fender, Belloni & Gallo 2004). Scaled with their respective mass ranges, the duration of the flare in Sw J1644+57 so far corresponds to only $\sim 10$–100 s in a typical Galactic BH. Further monitoring of the flux evolution over the next few months will help testing between the tidal disruption and state transition scenarios.

The scenario outlined above does not imply that every dip is due to oscillations and precession of the jet. Our most general interpretation is that dips correspond to phases when we are seeing slower and less collimated electrons along our line of sight in the jet. Even when the nozzle is steady, jets are subject to internal instabilities of magnetohydrodynamical nature. Internal shocks echo and self-intersect up and down the jet, producing standing patterns with a characteristic spacing that depends on the Mach number of the flow and the width of the jet. Jets also suffer an axisymmetric pinch instability, a non-axisymmetric helical instability, and other higher order harmonics of the helical instability (Hardee & Norman 1988; Norman & Hardee 1988; Hardee et al. 1992). Observed changes in the jet collimation and luminosity will depend on the interplay of the external driving oscillations (e.g. jet precession) and the resonant frequencies of the internal instabilities. The situation becomes even more complex if – as seems to be the case in Sw J1644+57 (Berger et al. 2012) – the jet has a broad Lorentz factor distribution rather than a single speed. With more arduously detailed modelling work (in the future), tested by long-term X-ray and radio monitoring (Berger et al. 2012), one might hope to infer something about the internal layering of the jet, and distinguish between internal- and external-driven jet variability.

5 CONCLUSION

We investigated the luminosity and spectral evolution of the peculiar X-ray source Sw J1644+57 using Swift/XRT data. Our structure function analysis shows that the large-amplitude variations in the light curve of the source are not simply stochastic fluctuations. In particular, the occurrence of at least some of the dips appears to follow some regular patterns characterized by multiples and fractions of a time interval $\tau \approx 4 \times 10^5$ s; visually, several prominent dips are spaced at $\approx 0.5 \tau \approx 2.2 \times 10^5$ s and $\approx 2 \tau \approx 9 \times 10^5$ s. After the plateau, the base period switched to $\tau \approx 1.4 \times 10^5$ s, but the scenario remains essentially the same. The X-ray spectrum outside the dips is always consistent with an absorbed power law, but its photon index evolves on a weekly/monthly time-scale, from $\Gamma \approx 1.8$ at the beginning of the decline phase to $\Gamma \approx 1.4$ at a later stage when the luminosity seems to level off. The X-ray spectrum is much softer during the dips, while there is no significant change in the absorption column density.

We proposed a scenario in which the synchrotron emitting jets, launched from a massive BH accreting a disrupted star, undergo both precession and nutation. The baseline flux in the keV band is direct synchrotron emission when the jet cone is in our line of sight; dips occur when the jet cone goes briefly and partially out of our line of sight. We argued that the synchrotron photons come from the optically thin jet ejecta during the initial high-luminosity, exponential decay phase; as the accretion power subsides, the dominant emission region becomes an opaque feature that is confined to a compact jet core. We attributed the fainter, steep-spectrum dip emission to a population of less energetic electrons, perhaps streaming in a cocoon surrounding the collimated jet core. Jet nutation and precession provide a natural explanation for the dip patterns in the X-ray light curve: in particular, their preferred occurrence at some
regular intervals, their occasional disappearance and subsequent reappearance, and the phase advance and delay of the dip centroids. In addition, internal jet instabilities can produce oscillations in the speed and cross-section of the jet flow and therefore a recurrent dipping behaviour. Long-term monitoring of the characteristic oscillation frequencies will be required to test whether they are due to internal or external drivers.

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NOTE ADDED IN PROOF

Shortly after our paper was accepted, Lei, Zhang & Gao (2012) submitted a preprint in which they obtain numerical solutions for a warped disc in Sw J1644+57, and propose a precessing Blandford–Znajek jet, collimated by an accretion disc wind launched near the Bardeen–Petterson radius.

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A2 Structure functions for unevenly sampled data

For continuous data, the order-

\[ S_{n}(\tau) = \langle (z(t + \tau) - z(t))^{n} \rangle \]

\[ = \frac{1}{T} \int_{-T}^{T} [z(t + \tau) - z(t)]^{n} \, dt. \]  

(A5)

For patchy, discretely binned data, we need to integrate contributions from each pair of potentially overlapping bins, piece by piece. If bin \( i \) overlaps with the offset copy of bin \( j \) then this pair contributes an amount \( I_{ij} \) to the numerator of the structure function,

\[ I_{ij} = I_{ij}(\tau) = \int_{T_{ij}}^{U_{ij}} [z(t + \tau) - z(t)]^{n} \, dt \]

\[ = \int_{T_{ij}}^{U_{ij}} [a_{i} t + a_{j} t + a_{ij} t + \beta_{-} - a_{i} t - b_{j}]^{n} \, dt, \]  

so that \( S_{n} = S_{n}(\tau) = W^{-1} \sum_{ij} I_{ij} \). The normalization factor \( W \) is the total duration of temporal overlaps between all pairs of bins:

\[ W = \sum_{ij} w_{ij}. \]  

(A7)

For \( a_{i} \neq a_{j} \) and \( A_{ij} \neq 0 \), the integral (A6) can be evaluated directly:

\[ I_{ij} = w_{ij} \int_{0}^{1} y^{n} \, d\lambda. \]

\[ = \frac{w_{ij}}{(n + 1)A_{ij}} [(A_{ij} + B_{ij})^{n+1} - B_{ij}^{n+1}]. \]  

(A8)

An alternative, binomial expansion proves to be more numerically stable in practice, especially where \( |A_{ij}| \) is small:

\[ I_{ij} = w_{ij} \sum_{k=0}^{n} \binom{n}{k} \frac{A_{ij}^{n-k} B_{ij}^{n-k}}{k + 1}. \]  

(A9)

A3 Determination of the uncertainties

If each bin \( k \) has a measurement \( z_{ik} \), with uncertainty \( \Delta z_{ik} \), then we obtain the uncertainty on the overall structure function by quadrature. Now, to propagate the uncertainties in the measurements \( z_{ik} \) to uncertainties in the structure functions \( S_{n}(\tau) \), one needs partial derivatives of each piece \( I_{ij} \) with respect to each observable \( z_{ik} \). It emerges that

\[ \frac{\partial I_{ij}}{\partial z_{ik}} = w_{ij} \sum_{k=0}^{n} \binom{n}{k} \left[ \frac{k}{k + 1} A_{ij}^{n-k} B_{ij}^{n-k} \frac{\partial A_{ij}}{\partial z_{ik}} \right] \]

\[ + \frac{n - k}{k + 1} A_{ij}^{n-k} B_{ij}^{n-k} \frac{\partial B_{ij}}{\partial z_{ik}}. \]  

(A10)

If we assume a zigzag data patching scheme \((z_{i+1} = z_{i} + \delta z_{i})\), then the relevant partial derivatives of \( A_{ij} \) and \( B_{ij} \) are

\[ \frac{\partial A_{ij}}{\partial z_{ik}} = \left( v_{ij} - \mu_{ij} \right) \delta_{i+1,k+1} + \left( v_{ij} - \mu_{ij} \right) \delta_{i,k} \]

\[ - \left( v_{ij} - \mu_{ij} \right) \delta_{i+1,k} + \left( v_{ij} - \mu_{ij} \right) \delta_{i,k+1}, \]  

(A11)

\[ \frac{\partial B_{ij}}{\partial z_{ik}} = \mu_{ij} \delta_{i+1,k+1} + (1 - \mu_{ij}) \delta_{i,k+1} \]

\[ - \mu_{ij} \delta_{i+1,k} + (1 - \mu_{ij}) \delta_{i,k+1}, \]  

where \( \delta \) is the Kronecker delta symbol. Now abbreviate

\[ A_{ij} = w_{ij} \sum_{k=0}^{n} \binom{n}{k} \frac{k}{k + 1} A_{ij}^{n-k} B_{ij}^{n-k}, \]

(A13)
\[ B_{ij} = w_{ij} \sum_{k=0}^{n} \binom{n}{k} \frac{n-k}{k+1} A_{ij}^{k} B_{n-k-1}, \]  

(A14)

and

\[ C_{1ij} = A_{ij} (v_{ij} - \mu_{ij}) + B_{ij} \mu_{ij}, \]  

(A15)

\[ C_{2ij} = -A_{ij} (v_{ij} - \mu_{ij}) + B_{ij} (1 - \mu_{ij}), \]  

(A16)

\[ C_{3ij} = -A_{ij} (v_{ij} - \mu_{ij}) - B_{ij} \mu_{ij}, \]  

(A17)

\[ C_{4ij} = A_{ij} (v_{ij} - \mu_{ij}) + B_{ij} (\mu_{ij} - 1). \]  

(A18)

It follows that

\[ \frac{\partial I_{ij}}{\partial z_{k}} = C_{1ij} \delta_{j,i+1} + C_{2ij} \delta_{i,j} + C_{3ij} \delta_{j,i+1} + C_{4ij} \delta_{i,j}, \]  

(A19)

By contracting the Kronecker deltas, we obtain

\[ \frac{\partial S_{n}}{\partial z_{k}} = \frac{1}{W} \sum_{ij} \frac{\partial I_{ij}}{\partial z_{k}} = \frac{1}{W} \sum_{i} (C_{1i,j-1} + C_{2i,j} + C_{3i,j} + C_{4i,j}) . \]  

(A20)

The four matrices \( (C_{1}, C_{2}, C_{3}, C_{4}) \) only need to be computed once for each choice of \( \tau \). If the uncertainties in the flux measurements are \( \Delta z_{k} \), the total uncertainty in the structure function is then given by

\[ (\Delta S_{n})^{2} = \sum_{k} \left( \frac{\partial S_{n}}{\partial z_{k}} \Delta z_{k} \right)^{2}. \]  

(A21)

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