NUCLEOSYNTHESIS IN CORE-COLLAPSE SUPERNOVA EXPLOSIONS TRIGGERED BY A QUARK–HADRON PHASE TRANSITION

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ABSTRACT

We explore heavy-element nucleosynthesis in the explosion of massive stars that are triggered by a quark–hadron phase transition during the early post-bounce phase of core-collapse supernovae. The present study is based on general-relativistic radiation hydrodynamics simulations with three-flavor Boltzmann neutrino transport in spherical symmetry, which utilize a quark–hadron hybrid equation of state based on the MIT bag model for strange quark matter. The quark–hadron phase transition inside the stellar core forms a shock wave propagating toward the surface of the proto-neutron star. This shock wave results in an explosion and ejects neutron-rich matter from the outer accreted layers of the proto-neutron star. Later, during the cooling phase, the proto-neutron star develops a proton-rich neutrino-driven wind. We present a detailed analysis of the nucleosynthesis outcome in both neutron-rich and proton-rich ejecta and compare our integrated nucleosynthesis with observations of the solar system and metal-poor stars. For our standard scenario, we find that a “weak” r-process occurs and elements up to the second peak (A ~ 130) are successfully synthesized. Furthermore, uncertainties in the explosion dynamics could barely allow us to obtain the strong r-process which produces heavier isotopes, including the third peak (A ~ 195) and actinide elements.

Key words: dense matter – nuclear reactions, nucleosynthesis, abundances – stars: neutron – supernovae: general

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1. INTRODUCTION

Nucleosynthesis from core-collapse supernovae is certainly responsible for the production of intermediate mass elements including the so-called alpha elements and a certain fraction of iron isotopes and their neighbors (the Fe-group nuclei). The lighter alpha elements from oxygen to silicon have contributions from hydrostatic burning which takes place during stellar evolutions, while the heavier ones and the Fe-group isotopes originate from explosive burning (Woosley & Weaver 1995; Thielemann et al. 1996; Woosley et al. 2002; Nomoto et al. 2006; Woosley & Heger 2007; Heger & Woosley 2010; Thielemann et al. 2011). A major open question is related to the source of heavy-elements beyond iron.

There have been strong expectations that the innermost layer of ejecta, close to the forming neutron star, remains neutron-rich and is a possible site for the r-process. For many years, the late neutrino-driven wind (NDW), following the actual explosion, seemed an adequate r-process site in core-collapse supernovae that formed a neutron star (Qian & Woosley 1996; Takahashi et al. 1994; Woosley et al. 1994). Such investigations were followed up by many parameterized calculations that explored the sensitivity of the most relevant r-process parameter, the neutron-to-seed ratio, via variations of entropy S, electron fraction (or number of proton per nucleon) Ye, and expansion timescale τ (Hoffman et al. 1997; Meyer & Brown 1997; Freiburghaus et al. 1999a; Farouqi et al. 2010). However, steady state wind models (Thompson et al. 2001; Wanajo 2006) showed that it is very hard to attain the required entropies. These results have been recently confirmed by fully hydrodynamical simulations (Arcones et al. 2007) that in addition showed that the presence of a reverse shock does not have any major impact on the neutron-to-seed ratio.

Furthermore, recent investigations noticed that the early NDW turns matter proton-rich, producing specific Fe-group isotopes and, in the subsequent vp-process, nuclei with a mass number up to A ~ 80–90 (Liebendorfer et al. 2003; Pruet et al. 2005, 2006; Fröhlich et al. 2006a, 2006b; Wanajo 2006). While it was initially hoped that there exists a chance that the late NDW still becomes neutron-rich (after its initial, early proton-rich phase), existing core-collapse calculations seem to indicate that the wind becomes even more proton-rich in the long-term evolution (Fischer et al. 2010, 2012; Hudepohl et al. 2010), although very recent investigations (Martínez-Pinedo et al. 2012; Roberts & Reddy 2012) related to the spectral evolution of νe and νe in medium might change this somewhat.

It was realized that the best chance to eject neutron-rich matter is to utilize material stemming from the initial collapse and compression, where electron captures turned it neutron-rich early in the explosion, before neutrino interactions have the chance to convert it into proton-rich matter in the NDW. Electron-capture supernovae, which explode without a long phase of accretion onto the proto-neutron star, apparently provide such conditions (Wanajo et al. 2011). However, the Ye’s obtained under such conditions do not support a strong r-process, which successfully reproduces the platinum peak of r-elements around A = 195.

An alternative explosive scenario as a possible site for the r-process has been suggested by Jaikumar et al. (2007), where after a supernova explosion a quark–hadron phase transition inside the neutron star can eject very neutron-rich material from the neutron star surface. This scenario has been referred to
as a quark–nova. In the present paper, we follow a different approach and investigate core-collapse supernova explosions that are triggered by a quark–hadron phase transition during the early post-bounce phase (for details, see Sagert et al. 2009; Fischer et al. 2011) and their nucleosynthesis features. Under such conditions, zones which are initially neutron-rich can be (promptly) ejected without experiencing the strong effects of the neutrino flux that comes from the central proto-neutron star.

In the following sections, we discuss the supernova explosion model and the nuclear physics inputs utilized for the nucleosynthesis calculations in Section 2, the conditions experienced and the resulting ejecta in Section 3, and give a detailed analysis of the ejecta composition in Section 4, followed by conclusions, also in comparison to alternative r-process sites, in Section 5.

2. METHODOLOGY AND NUCLEAR PHYSICS INPUT

We explore nucleosynthesis in core-collapse supernovae that are triggered by a deconfinement phase transition during the early post-bounce phase. The explosion models have been discussed in detail by Fischer et al. (2011). In this section, we summarize the main features of the explosion models and the input physics of the nuclear reaction network utilized for nucleosynthesis.

2.1. Hydrodynamics and Equation of State

A self-consistent supernova explosion model, which we adopt to investigate nucleosynthesis in the present work, has been carried out by using the AGILE-BOLTZTRAN code. This numerical code is based on general-relativistic radiation hydrodynamics in spherical symmetry with an adaptive grid and employs a three-flavor Boltzmann neutrino transport (Liebendörfer et al. 2004) with detailed microphysics, e.g., a realistic nuclear equation of state (EOS), weak processes, and (other) nuclear reactions. For the current study, the standard weak processes were considered as listed in Table 1 of Fischer et al. (2011).

The baryonic EOS in supernovae needs, in general, to be known for the following three intrinsically different regimes:

1. At temperatures below 6 GK (≥0.5 MeV), the baryon EOS is dominated by heavy nuclei and their abundances, determined by individual nuclear reactions which are not necessarily in equilibrium. In Fischer et al. (2010), we included a nuclear reaction network, consisting of 20 nuclei, which allows us to simulate a large domain of the progenitor up to the helium layer and is utilized to predict the amount of energy generation by explosive nuclear burning.

2. At temperatures above 6 GK (≥0.5 MeV), the nuclear statistical equilibrium (NSE) can be applied, where the baryonic EOS from Lattimer & Swesty (1991) and Shen et al. (1998) are commonly used in supernova simulation studies.

3. Above the nuclear matter density, the state of matter is highly uncertain. There exists the possibility of a deconfinement phase transition. Therefore, we extended the hadronic EOS by Shen et al. (1998) at high densities and temperatures, making use of a quark EOS based on the bag model for strange quark matter. For the first-order phase transition between hadronic and quark phases, we applied Gibbs conditions, leading to a mixed phase during the transition. This results in a continuous phase transformation. Details of the quark–hadron hybrid EOS are discussed in Fischer et al. (2011).

Besides the contributions from electrons and positrons as well as photons, Coulomb corrections to the EOS are added by the method of Timmes & Arnett (1999).

For the current nucleosynthesis predictions, we select the explosion calculations of the 10.8 $M_\odot$ progenitor model, where a quark–hadron hybrid EOS was used with an early phase transition to quark matter close to normal nuclear matter density (labeled EOS2, second line of Table 2 in Fischer et al. 2011). We chose this model because it has an explosion energy consistent with the expected order of magnitude of $10^{51}$ erg (see the second line of Table 3 in Fischer et al. 2011). The maximum gravitational mass for this EOS is 1.5026 $M_\odot$. Though it is in agreement with the highest precisely known mass of a compact star, the Hulse–Taylor pulsar of 1.44 $M_\odot$, recent mass limits for the physical EOS are based on the millisecond pulsars J1903+0327 with $M = 1.667 \pm 0.021 M_\odot$ (Freire et al. 2011) and J1614–2230 with a high mass of $M = 1.97 \pm 0.04 M_\odot$ (Demorest et al. 2010). The inclusion of corrections from the strong interaction coupling constant can stiffen the quark EOS and lead to higher maximum masses (see, e.g., Schertler et al. 2000; Alford et al. 2005; Sagert et al. 2010; Weissborn et al. 2011).

The physical conditions for a possible quark–hadron phase transition in the proto-neutron star are highly uncertain. Therefore, Fischer et al. (2011) also constructed a quark–hadron hybrid EOS which includes corrections from the strong interaction coupling constant. They showed that such an EOS, with a maximum mass of 1.67 $M_\odot$ and a phase transition to quark matter close to nuclear saturation density (see EOS3 in Tables 2 and 3 in Fischer et al. 2011), leads to a qualitatively similar explosion scenario in spherical symmetry as obtained in the explored models with several EOSs that have lower maximum masses. Note that the different post-bounce times for the onset of deconfinement, and hence for the onset of the explosion, lead to different proto-neutron star structures. In general, a delayed phase transition at higher densities translates to a longer mass accretion phase (for the same progenitor). It results in a more massive proto-neutron star with a steeper density gradient at its surface and a lower $Y_e$ at the onset of the explosion triggered by the phase transition. An earlier phase transition and less steep density gradient would result in a slower expansion and a slightly higher $Y_e$.

This has important consequences for the nucleosynthesis of the ejected material since expansion timescale and enclosed mass, and also neutrino luminosities and spectra, depend on these aspects (for a detailed discussion, see Fischer et al. 2011) and on the behavior of EOS1 and EOS2 in their Figure 17.

Weissenborn et al. (2011) recently showed that it is possible to obtain a quark–hadron hybrid EOS that allows for both a maximum mass larger than 2 $M_\odot$ and a low critical density for the appearance of quark matter. Whether such a quark–hadron hybrid EOS will result in a similar dynamical evolution as discussed in Fischer et al. (2011) will be examined in future simulations.

2.2. Explosion Scenario

The supernova post-bounce evolution is characterized by mass accretion causing a continuous rise of the central density. Once the central density exceeds the critical density for the onset of deconfinement, the quark–hadron phase transition takes place, leading to the appearance of a quark–hadron mixed phase. Through this process, quark matter appears in the supernova core where the highest densities are experienced. The timescale for
the appearance of quark matter is given by the timescale for the central density to rise. This depends on the progenitor model, which determines mass accretion rates, and the hadronic EOS. Note that the EOS in the mixed phase is significantly softer than in hadronic and pure quark phases. It is a consequence of the assumed first-order phase transition. Mass accretion from the outer layers of the progenitor onto the central supernova core leads to a continuous rise of the central enclosed mass. When the critical mass (given by the hybrid EOS) of the configuration is obtained, it becomes gravitationally unstable and the supernova core begins to contract. The contraction proceeds into a collapse which raises the density and converts the hadronic core into quark matter at around the center. A massive pure quark core forms at the center, where the EOS stiffens and the collapse halts, and an accretion shock forms. The shock wave propagates out of the high-density supernova core, remaining as an accretion front with no matter outflow. Once it reaches the outer layers of the central core, where the density drops over several orders of magnitude, the accretion front accelerates and turns into a dynamic shock with matter outflow. This moment also determines the onset of an explosion for supernova models which would otherwise not explode in spherical symmetry, based on explosion mechanisms discussed so far. Finally, at distances on the order of 100 km, the expanding shock wave merges with the standing shock from the initial core bounce at nuclear densities, which was unaffected by the dynamics occurring in the supernova core.

When the (second) shock reaches the neutrino spheres, an additional millisecond neutrino burst is released. It appears in all flavors, however, it is dominated by $\nu_e$ and $\bar{\nu}_e$, in contrast to the $\nu_{\mu}/\tau$-deleptonization burst related to the early bounce shock propagation across the neutrino spheres between 200 and 500 ms after core bounce. This second neutrino burst is of particular interest for water-Cherenkov neutrino detectors, which are more sensitive to $\bar{\nu}_e$ than to $\nu_e$. Dasgupta et al. (2010) demonstrated that the currently operating generation of water-Cherenkov neutrino detectors (e.g., Super-Kamiokande and IceCube detectors) can resolve such millisecond neutrino bursts as the explosion models by Fischer et al. (2011).

The matter considered for nucleosynthesis studies of heavy elements (see Section 3) belongs originally to the inner parts of the silicon and sulfur layers of the 10.8 $M_\odot$ progenitor from Woosley et al. (2002), with a temperature and electron fraction of 3 GK and $Y_e \approx 0.5$, respectively, at 800–1000 km from the center on the pre-collapse phase. During the collapse and the explosion, material contracts and is heated by the shock to temperatures exceeding 100 GK and hence completely dissociates into free nucleons. At high densities, weak processes, mainly electron captures, establish a very low proton-to-baryon ratio $Y_p \approx 0.1$ during the core collapse. Further evolution is discussed in detail in Section 3.

2.3. Nuclear Reaction Network

The nuclear reaction network utilized for the following nucleosynthesis simulations of the ejecta is an extension of previous ones, which have already been described in detail (see Nishimura et al. 2006; Fujimoto et al. 2008). The network includes more than 4000 nuclei from neutrons and protons up to fermium with atomic number $Z = 100$ (for detail, see Table 1 in Nishimura et al. 2006) and includes proton-rich isotopes as well as neutron-rich ones far from stability. It includes two- and three-body reactions, decay channels, and electron as well as positron capture (for details, see network A in Fujimoto et al. 2007). Spontaneous and beta-delayed fission processes are applied, based on the finite range droplet mass model (Møller et al. 1995). Experimentally determined masses (Audi & Wapstra 1995) and screening effects for all relevant charged-particle reactions. Experimentally determined masses (Audi & Wapstra 1995) and reaction rates are adopted if available. Otherwise, theoretical predictions for nuclear masses, reaction rates, and beta-decays are applied, based on the finite range droplet mass model (Møller et al. 1995). Spontaneous and beta-delayed fission processes (Staudt & Klapdor-Kleingrothaus 1992) are taken into account. We adopted the empirical formula for fission fragments by Kodama & Takahashi (1975).

We also employ neutrino interactions with matter in order to include dominant weak interactions affecting the evolution of the overall proton/nucleon ratio $Y_e$. For (anti-)electron–neutrino captures by nucleons, we adopt reaction rates derived by Qian & Woosley (1996) but ignore any reactions with heavy isotopes because the amount of neutrino capture is negligible for the early phase of nucleosynthesis. The neutrino fluxes, resulting from the detailed neutrino-radiation hydrodynamics calculation described in the previous subsection, are utilized to determine the actual rates as a function of time. These reaction rates depend on the distance from the proto-neutron star and the mean energy and luminosity of neutrinos emitted from the proto-neutron star. It depends on the structure and the evolution, which is sensitive to the EOS, and the precise evolution history of ejected matter including the early phase of the core bounce. Thus, this is different from the treatment of other nuclear reaction rates, which are determined only by local thermodynamic conditions and density and temperature.

3. NUCLEOSYNTHESIS IN THE EJECTA

3.1. Dynamic Evolution of Mass Zones

In order to calculate the nucleosynthesis evolution of ejected matter within a postprocessing approach, the dynamic evolution is required in radial Lagrangian mass zones. For this reason, the evolution determined with the radiation hydrodynamics code AGILE-BOLTZTRAN (see Mezzacappa & Bruenn 1993a, 1993b, 1993c; Liebendorfer et al. 2001a, 2001b), which is based on an adaptive grid, was mapped on a Lagrangian grid of 120 mass zones. This provides the Lagrangian evolution of physical quantities, such as density, temperature, electron fraction, and velocity of the ejected material, and in addition the neutrino fluxes experienced as a function of time.

The mass zones which are ejected in the explosion are classified in three different categories related to their ejection process and thermodynamic quantities. As listed in Table 1, zones 001 to 120, given with the ejection timescale after bounce ($t_e$) and the final $Y_{e,NSE}$, which is $Y_e$ at the end of NSE (below $T = 9$ GK), cover the material from the surface of the inner core at 1.48000 $M_\odot$ to layers with a corresponding mass of 1.49482 $M_\odot$. They are also shown with respect to their mass as well as $Y_e$-distribution in Figure 1.
These zones coincide with the matter discussed at the end of Section 2.2, where at high densities a \( Y_e \) decrease down to even 0.02 has been noticed. The evolution of these mass zones in time is displayed in Figure 2. Zones 001 to 014 are not ejected within 0.5 s after the core bounce. These zones preserve the original low-\( Y_e \) obtained during collapse and shock wave propagation. As they are not ejected, we ignore them in all further nucleosynthesis discussion, including all matter originating from regions at smaller radii. In Figure 2, they are displayed in black. Zones 015 to 019 are ejected in the so-called NDW, shown in red. Their \( Y_e \) is strongly affected by neutrino interactions, turning this matter proton-rich. Zones 020 to 050 (displayed in green) have stalled from infall after shock formation and are ejected thereafter due to neutrino heating and dynamic effects (Fischer et al. 2011). The adjacent zones 051 to 120, \( Y_e \) stays essentially constant at \( \approx 0.5 \) and the enclosed mass continues to be proportional to mass zone numbers.

(A color version of this figure is available in the online journal.)

Figure 2. Top: radial trajectories of mass elements as a function of time after bounce. The colors indicate the properties of these mass elements: black, red, green, and blue lines refer to matter which is either (black) not ejected, (red) part of the neutrino-driven wind, (green) initially stalled matter which gets boosted by the wind, and (blue) matter which experiences a prompt ejection. Bottom: evolution of \( Y_e \) as a function of time after the core bounce. The deconfinement phase transition happens about 0.4 s after this initial bounce, causing the explosion and ejection of matter. The colors are the same as in the top panel.

(A color version of this figure is available in the online journal.)

As shown in the bottom part of Figure 2, the blue and green zones are neutralized during the collapse via electron capture to various degrees, depending on the maximum density attained. Thus, the main feature is that a strong compression during infall leads to high densities (at still low entropies, i.e., highly degenerate matter) with large electron Fermi energies which endore electron captures and a strong neutronization of matter with a small \( Y_e \). Their \( Y_e \)-values range from 0.35 to 0.5. The prompt or quasi-prompt ejection does not change this value (with minor effects on the innermost zones, being partially affected by the NDW). The effect of neutrino and anti-neutrino exposure from the core leads also to an increase of \( Y_e \), as discussed before. Therefore, the major point in favor of an \( r \)-process is a fast expansion of that material having two aspects: (1) timescales are shorter than needed for attaining weak equilibrium and (2) matter moves fast to larger radii where the effect of neutrinos vanishes \( (1/r^2) \). The mass zones in red experience a similar effect in their early evolution during collapse; but the later evolution leads to values of \( Y_e \) exceeding 0.5. This is similar to recent studies of the NDW (see the Introduction and Fischer et al. 2010), where similar neutrino and anti-neutrino spectra and flux intensities favor proton-rich matter due to the neutron–proton mass difference, resulting in different energies available for the neutrino/anti-neutrino captures. As the neutrino luminosity is still high in the ejection phase, we expect \( v+p \)-process nucleosynthesis. Finally, non-ejected mass zones (black) can also initially experience interaction with the neutrino flux and turn proton-rich while still at larger radii and small(er) densities. Once they settle on the surface of the neutron star at high densities, capture of degenerate electrons dominates over the neutrino effects, and they turn neutron-rich again.

The thermodynamic conditions (density, temperature, and entropy), which are responsible for the nucleosynthesis results, are shown in Figure 3 for the ejected mass zones. These figures indicate a temperature, density, and entropy maximum when the quark–hadron phase transition occurs, which causes a second core bounce (about 0.4 s after the first bounce at nuclear

(A color version of this figure is available in the online journal.)
1. Neutrinos from the Proto-neutron Star

The properties of the neutrino and anti-neutrino flux (luminosities, average energies, and neutrino sphere radii) can be found in Figure 4. It is clearly seen that the initial bounce (0 s) at nuclear densities leads to a neutrino burst due to electron captures, while the second shock wave caused by the quark–hadron phase transition (at 0.4 s) also produces anti-neutrinos. From that point on in time, the neutrino and anti-neutrino luminosities are comparable (slightly smaller for anti-neutrinos). The average energies are larger for anti-neutrinos than for neutrinos, but the difference remains less than 4 MeV. Neutrino and anti-neutrino captures determine the neutron/proton ratio due to the reactions

\[ \bar{\nu}_e + p \rightarrow n + e^+ \quad \nu_e + n \rightarrow p + e^- . \]

Based on the neutron/proton mass difference of \( \Delta = 1.293 \text{ MeV} \), Fröhlich et al. (2006a) could show (see their Equation (4)) that with the use of Equations (64a) and (64b) in Qian & Woosley (1996), \( Y_e > 0 \) in the case that the difference between the mean anti-neutrino and neutrino energies fulfills \( \epsilon_{\bar{\nu}_e} - \epsilon_{\nu_e} < 4 \Delta \), with \( \epsilon = \langle E^2 \rangle / \langle E \rangle \) and where \( \langle E \rangle \) is the mean energy and \( \langle E^2 \rangle \) is the square value of the root-mean-square (rms) energy. Therefore, \( Y_e > 0.5 \) is obtained if the timescale for neutrino/anti-neutrino captures is shorter than the dynamic timescale. Thus, for all conditions discussed here, where neutrino and anti-neutrino captures are responsible for the \( n/p \) ratio, proton-rich conditions are attained, i.e., \( Y_e > 0.5 \). That is exactly what is seen in Figures 2 and 4 for mass zones which experience essential neutrino fluxes (weighted by \( 1/r^2 \)) at radii of about 100 km. It is related to the spectral evolution of \( \nu_e \) and \( \bar{\nu}_e \) after the onset of explosion and has been discussed in detail in Fischer et al. (2012). For matter at larger radii (about 1000 km), the timescale for this process is too long and minor \( Y_e \) changes occur, i.e., the initial \( Y_e \) from the collapse phase is retained. Matter at smaller radii, on top of the neutron star, experiences high densities and electron Fermi energies, where electron captures dominate which make matter neutron-rich.

Figure 5 underlines this effect due to neutrino interactions or electron capture. All outer mass zones keep their original \( Y_e \),
which is due to electron capture at high densities during the collapse, and ranges from about 0.48 (further out) to 0.32 (for the inner quasi-prompt ejected matter). Material which fell initially onto the surface of the neutron star and is then ejected via the NDW has been turned proton-rich by neutrino and antineutrino captures with values up to \(Y_e\) from the infall/compression phase. (A color version of this figure is available in the online journal.)

Figure 5. \(Y_e\) and entropy \(S\), which set the conditions for explosive nucleosynthesis at the time of matter ejection. The innermost ejected zones are proton-rich due to the effect of the neutrino-driven wind, which also heats matter efficiently, leading to high entropies. The outer mass zones, ejected in a more prompt fashion, keep their original (slightly neutron-rich) \(Y_e\) from the infall/compression phase.

3.3. Nucleosynthesis Results

In the following, we show final nucleosynthesis results for a number of typical mass zones. In order to get a rough idea about the results of explosive nucleosynthesis, one can utilize either maximum densities and temperatures prior to an adiabatic expansion or the entropies attained in the expanding matter (in radiation-dominated regimes \(5 \propto T^3/\rho\).

Comparing entries in Figure 5 of Thielemann et al. (1990) and Figure 3 of Thielemann et al. (1996) leads to the conclusion that (1) these are typical conditions for an alpha-rich freezeout from explosive Si-burning and (2) one would expect the remaining alpha mass fractions after charged-particle freezeout of the order of 20\%-100\%. One should consider, however, that those calculations were performed for hydrodynamic (i.e., free fall) expansion timescales, which can differ from the actual situation, and a value of \(Y_e = 0.4988\), i.e., matter neither neutron nor proton-rich. Therefore, we expect the following changes: (1) higher/lower entropies within the given variety will lead to higher/lower remaining alpha-fractions; (2) higher \(Y_e\), i.e., more proton-rich matter causes an alpha-rich charged-particle freezeout with remaining free protons, which can thereafter lead to a \(vp\)-process, if a sufficient flux of electron anti-neutrinos is still present; and (3) smaller \(Y_e\)’s, i.e., more neutron-rich matter is permitted to bypass the slower triple-alpha reaction via the faster \(aan\)-reaction in order to produce heavier nuclei, and a reduction in the remaining alpha-fraction is expected. In addition, free neutrons remain after the charged-particle freezeout. With respect to this latter aspect, we also expect this additional behavior: higher entropies and lower \(Y_e\)’s lead to a larger neutron/seed ratio, seed nuclei being the heaviest nuclei formed after charged-particle freezeout, and permit therefore more neutron captures on these seed nuclei. Dependent on the neutron-to-seed ratio, this could lead to light, medium, or strong \(r\)-processing, producing nuclei in the first, second, or third \(r\)-process peaks, around \(A = 80, 130,\) or 195, depending on the actual \(n/seed\) ratio attained.

In Figure 6, the properties of mass zones 020 to 120 are summarized, i.e., those with a \(Y_e < 0.5\) that experience neutron-rich conditions to a varying degree. Properties (1), i.e., the degree of alpha-rich freezeout, and (3), the resulting neutron/seed ratio, are displayed. We see a complex dependence of these properties on the entropy \(S\), \(Y_e\), expansion timescale \(\tau\), plus further complications from reheating and re-expansion that do not fit a simple expansion interpretation. For similar \(Y_e\)’s, the remaining alpha-fraction increases with entropy, as expected, when looking at the behavior of mass zones 080 to 120. Then, following mass zones further in, the decrease in \(Y_e\) dominates, which permits passage to the alpha-to-carbon bottleneck more efficiently, via the \(aan\)-reaction, and the remaining alpha-fraction vanishes. As is known from moderately neutron-rich NDW simulations, none of the entropies encountered here lead to sizable neutron/seed ratios. For such low entropies, only a strongly neutron-rich initial composition permits large(r) neutron/seed ratios. This is what can be noticed when following mass zones from 070 down to 040, where the lowest \(Y_e\)’s are encountered. Mass zones 020 to 040 experience a more complicated history, initial expansion after shock passage, partial fallback, and then final ejection and further expansion. Here, the neutron/seed ratio after the first charged-particle
freezeout is of particular importance for the production of heavy elements.

The reheating leads to partial photodisintegration of heavy elements, the production of alphas, and the buildup toward nuclei with mass numbers around \( A = 90-110 \) during the final expansion. The neutron/seed ratio at this second charged-particle freezeout (boost) is rather a measure for local rearrangements of matter.

The maximum neutron/seed ratio of slightly above 10, obtained over the complete range of ejected mass zones, does not support conditions to produce the third \( r \)-process peak; in fact, only a small production of the second peak is expected. The effect of the “boost,” i.e., the second reheating and expansion in mass zones 20–40, rearranges/reshapes the abundance distribution via photodisintegrations and captures, but does not alter this conclusion.

With this background, we have a look at the final abundances of representative mass zones, displayed in Figure 7. We see in the outer layers the remaining alpha-fractions beyond 60%. These are regions that experience entropies of \( S = 33-50 \) \( k_b \) per baryon and \( Y_e 's close to 0.5 \) and see vanishing neutron/seed ratios. Thus, we essentially expect the production of the Fe-group up to \( A = 50-70 \). This can be observed in the last two subfigures of Figure 7 (zones 80 and 120). Mass zones 60 and 70, which experience the highest entropies and moderately decreased \( Y_e 's, can move matter up to and (slightly) beyond \( A = 90 \) (for mass zone 70 still with a large fraction of matter in the Fe-group), mostly due to a more neutron-rich (lower \( Y_e \)) charged-particle freezeout and not due to further neutron processing (see neutron/seed ratio in Figure 6). One can also see a variation in the final carbon fraction, underlining how effective the bridging of the alpha-to-carbon bottleneck of reactions is in comparison to subsequent capture reactions to heavier nuclei. At smaller radii (mass zones 020 to 051 and \( Y_e 's \) as small as 0.33), the \( A = 130 \) peak starts to be populated. This is due to the neutron/seed ratio of up to 10 attained after charged-particle freezeout. For the mass zones 20–45, abundances are shown after the first expansion (dashed) and after reheating/boost (solid), which is characterized by some photodisintegration of heavy nuclei, the appearance of \( ^4\)He, and further processing of nuclei beyond the Fe-group (see also Figure 8). To summarize the results of all the mass zones with \( Y_e < 0.5 \), we note that none of these zones produce matter beyond \( A \sim 130 \), nor show the 130 peak dominating abundances.

Deeper mass zones, ejected via the NDW, turn proton-rich and experience entropies as high as 85 \( k_b \) per baryon. These are conditions where we expect a \( v_p \)-process (Fröhlich et al. 2006b; Pruet al. 2006; Wanajo 2006). This can be seen in the first three panels of Figure 7, where dashed lines show abundances without the inclusion of the \( v_p \)-process and solid lines show the final results after \( v_p \)-processing. While in terms of total mass fraction the production of nuclei beyond the Fe-group is not
Figure 8. Top: the comparison of results with (solid) and without (dashed) the effect of reheating and second expansion (boost) integrated over the whole range of mass zones 20–50. Bottom: the ratios of the two cases, based on the full hydrodynamic evolution with reheating (boost) and the neglect of reheating around 1.5 s. The reheating leads to photodisintegrations, a strong appearance of $^4\text{He}$, and a reshaping of the heavy-element distribution.

(A color version of this figure is available in the online journal.)

Figure 9. Resulting nucleosynthesis for the entire mass zones in the neutrino-driven wind, experiencing a $\nu_p$-process. The result is shown for two options: (a) including the anti-neutrino captures which turn protons into neutrons in the late phase of nucleosynthesis and permit them to overcome the $^{64}\text{Ge}$ beta-decay bottleneck via an $(n,p)$-reaction (filled red circles), (b) neglecting this effect (open black circles). It can be seen that the inclusion of anti-neutrino reactions enhances abundances of nuclei heavier than $A = 64$ and permits the production of nuclei up to $A = 80–90$.

(A color version of this figure is available in the online journal.)

too impressive, Figure 9 displays this more prominently, where the overproduction ratio over solar is plotted. In the proton-rich environment, anti-neutrino captures on free protons produce neutrons and permit them to overcome the $r$-process waiting point $^{64}\text{Ge}$ via an $(n,p)$-reaction, winning against a slower $\beta^+$-decay. In this way, nuclei up to $A = 80–90$ can be produced on the proton-rich side of stability. The comparison of the black and red bullets indicates the strength of this process.

Figure 10. Overview of dominating conditions, i.e., abundances of a few key nuclei after charged-particle freezeout, as a function of radial Lagrangian mass, with variations from (a) typical explosive Si-burning products and an alpha-rich freezeout in the outer zones to (b) an increasing remaining neutron abundance after charged-particle freezeout, permitting a weak $r$-process, down to (c) proton-rich neutrino-driven wind ejecta, permitting the onset of a $\nu_p$-process.

(A color version of this figure is available in the online journal.)

4. SURVEY AND INTEGRATED COMPOSITION

After having discussed the individual composition ejected from different positions in the exploding model, we want to give a final survey of the conditions attained in all mass zones of explosive Si-burning which are affected by the explosion mechanism (here, the deconfinement phase transition). The discussion of nucleosynthesis in layers further out is only affected by the energy in the shock wave, as has been discussed extensively in the literature (Thielemann et al. 1996), and will not be repeated here. Finally, we also discuss the overall features of the integrated yields (of these inner mass zones, close to the explosion mechanism). The survey is displayed in Figure 10 which features abundances after charged-particle freezeout, and thus serves as the setting for the final nucleosynthesis features if free neutrons or protons remain in sizable fractions.
Essentially, all mass zones have total entropies in excess of $S = 30$ $k_B$ per baryon. In the outer mass zones with a $Y_e$ close to 0.5, this produces high alpha-fractions plus dominant $^{56}$Ni. Moving somewhat further in with slightly increasing entropies, noticeable amounts of $^{64}$Ge are produced as well, with the $^{64}$Ge/$^{56}$Ni being a measure of entropy. Decreasing $Y_e$, i.e., having more neutron-rich conditions, changes the initially pure alpha-rich charged-particle freezeout to an alpha-rich freezeout with sizable abundances up to $A = 90$. A further decrease in $Y_e$ causes remaining free neutrons, which permit an additional sequence of neutron captures. The decrease of $Y_e$ down to 0.33 leads to a charged-particle freezeout with vanishing alpha-fractions but a sufficient amount of free neutrons, which later allow the production of nucleosynthesis ejecta in the mass $A = 130$ peak. The mass zones which are affected by a reheating boost are characterized by photodisintegrations and a second charged-particle freezeout with remaining alpha-fractions. Finally, the innermost proton-rich zones, with higher entropies of about $S = 85$ $k_B$ per baryon and experiencing a continuous neutrino flux, show an alpha-rich and proton-rich freezeout with $Y_e$‘s up to 0.55. This causes a $\nu p$-process after charged-particle freezeout, which is permitted by neutron production via anti-neutrino captures on free protons. This process will produce nuclei up to $A = 90$, but on the proton-rich side of stability, especially Sr, Y, and Zr isotopes.

After this survey of the conditions at charged-particle freezeout, combined with the final ejecta composition as a function of radial mass coordinate as discussed in the previous section, we want to give an integrated presentation for these inner mass zones which experience conditions for the possible formation of nuclei beyond the Fe-group. Figure 11 (top) shows the composition for this range in mass numbers in comparison to solar $r$-abundances. As we do not yet know the frequency of such events, i.e., which range of the initial mass function of stellar masses leads to these types of explosions, we show a scaling normalized to the $A \sim 100$ mass region (where the dominant abundances are obtained). The bottom part of Figure 11 shows the individual contributions to the overall abundances by the different mass zones as presented in Table 1 and Figure 1, and shown in different colors in Figures 2 and 3 as well as Figures 5–7. The high end of the abundance distribution in the prompt (blue, dashed) as well as the delayed (boosted) ejecta (green, solid) are due to the most neutron-rich conditions, with $Y_e$ close to 0.33. The outermost ejected mass zones with $Y_e$ closer to 0.5 contribute to the Fe-group and matter up to $A = 80$ (lower range of mass numbers of blue dashed line). The NDW (red line) with slightly proton-rich ejecta ($Y_e = 0.55$) produces significant abundances only up to $A = 64$ if the same normalization for the relevant mass zones is used (see, however, also Figure 9).

It is clearly visible that, first of all, objects like these supernovae, exploding by a mechanism based on EOSs with a low-density quark–hadron phase transition, only experience a weak $r$-process in ejected mass zones which were neutronized during collapse. There is no matter produced in the third $r$-process peak. As shown in Figure 11, if we normalize the abundance curve with the solar $r$-process pattern at $A = 100$, we can infer that the amount of further heavy elements ($A > 100$) is rather small and more than 10% reduction in $Y_e$ is required to produce the second $r$-process peak, i.e., $A = 130$. The major production affects the atomic mass range from $A = 80$ to 115, curiously, also reproducing a minimum at $A = 97$–99. Thus, the type of events discussed here contribute to the whole mass region beyond the Fe-group up to $A = 115$ in a significant way, and are accompanied by minor contributions to the second $r$-process peak at $A = 130$.

5. MODEL UNCERTAINTIES

5.1. Equation of State Uncertainties

The major uncertainty in the present calculations is expected given the uncertain properties of the EOS, especially the quark–hadron phase transition which is at the origin of the explosion mechanism discussed here. This was already reviewed extensively in Section 2.1. The analysis done by Fischer et al. (2011), with variations in the properties of the phase transition, led to different post-bounce times for the onset of the explosion and different neutron star structures. Later transitions at higher densities cause more massive progenitors with steeper density gradients at the surface. The standard case of the present paper corresponds to EOS2 in Figure 17 of Fischer et al. (2011), i.e., a late($\nu$) explosion with a steep($\rho$) density gradient and thus a fast expansion. Variations toward the properties of EOS1, with an earlier explosion, would cause slower expansions. Therefore, we performed test (nucleosynthesis) calculations with slower expansions for a specific mass zone (here, zone 51, see also Figure 7) which provided among the best $r$-process conditions in our standard case. Figures 12 and 13 show variations with exponential density expansions fitted to the standard case.
timescales by factors of 2, 5, and 10 (choosing the temperature evolution according to EOS2 and exponential density expansions fitted to this case ($f = 1$) as well as slower expansions with longer expansion timescales by factors of 2, 5, and 10. (A color version of this figure is available in the online journal.)

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Figure 12. Density evolution as a function of time. Shown is the standard case with the original explosion simulation according to EOS2 and exponential density expansions fitted to this case ($f = 1$) as well as slower expansions with longer expansion timescales by factors of 2, 5, and 10. (A color version of this figure is available in the online journal.)

In typical NDW environments for given $S$ and $Y_e$, a fast(er) expansion leads to a strong(er) alpha-rich freezeout, and thus more alpha particles and less seeds and a higher neutron/seed ratio, promoting the options for a stronger $r$-process. However, in the mass zones of interest here, the $Y_e$ is quite low and the remaining alpha-fraction is nearly negligible. This feature was discussed extensively in Section 3.3 with respect to Figures 6 and 7. We see the effect in Figure 14 that the fastest expansion ($f = 1$) shows the highest remaining alpha-fraction, but only of the order of $10^{-4}$. This behavior lowers the initial seed abundance after charged-particle freezeout by the same amount, which is negligible. This causes essentially the same seed abundances and neutron/seed ratio for all calculations with different expansion speeds ($f = 1$–10) and cancels this dominant effect in typical NDW environments. In fact, the slowest expansion leads to the highest abundances at $A = 130$. Here, a second-order effect seems to take over. The different density and temperature conditions for slower expansions lead to an apparently slightly more neutron-rich $r$-process path, encountering smaller beta-decay half-lives that permit them to proceed faster to heavier nuclei. This behavior, as shown in Figure 14, indicates a slightly stronger (weak) $r$-process for the slower expansions. However, the effect is not strong, and is only clearly visible for $f = 10,$ which is larger than the uncertainty encountered in our EOS variations.

5.2. $Y_e$ Uncertainties

One can argue that there may exist some uncertainty in the weak interactions (electron/positron captures and neutrino captures; see, e.g., Langanke & Martínez-Pinedo 2003; Janka et al. 2007; Cole et al. 2012) that determine $Y_e$, especially due to recent developments that include charged-current rates that are consistent with the EOS (for details, see Martínez-Pinedo et al. 2012; Roberts & Reddy 2012). These very recent preliminary investigations include medium effects for the (electron) neutrino and anti-neutrino capture reactions, which lead to changed reaction $Q$-values by adding nucleon interaction potential differences for neutrons and protons, and, as a result, enhancing the difference between average anti-neutrino and neutrino energies. This causes a change in $Y_e$. All our earlier discussions emphasized that the influence of the neutrino flux from the proto-neutron star would cause an increase in $Y_e$. The preliminary analysis of such effects by Martínez-Pinedo et al. (2012) and Roberts & Reddy (2012), which were not included in the present calculations, shows that the $Y_e$ increase is weakened or that even moderately neutron-rich conditions ($Y_e \lesssim 0.5$) can result.

For this reason, we also repeated the present nucleosynthesis calculations with variations in the initial $Y_e$ for the mass zones experiencing prompt and delayed explosions, according to the following formula:

$$Y_{e, \text{cor}} = 0.5 + (Y_e - 0.5) \times \left(1 + \frac{P_{\text{cor}}}{100}\right),$$

where the $Y_{e, \text{cor}}$’s are the corrected ones and $P_{\text{cor}}$ denotes the percentage of uncertainty in deviations of $Y_e$ from the symmetric value 0.5, which increases these deviations from 0.5. This lowers the initially only moderately neutron-rich $Y_e$’s in regions that already produced $A = 130$ nuclei. The nucleosynthesis results are presented in Figures 11 and 15 and show the options of obtaining a full or weak $r$-process. However, we expect that any uncertainties beyond 20% are unrealistic for the explosion model we adopt in the current work.

As is obvious from the discussion above, only a “weak” $r$-process can be supported by the nucleosynthesis conditions found in the explosion mechanism discussed and presented here,
and one might wonder whether such conditions support abundance features found in “weak r-process” low-metallicity stars as observed by Honda et al. (2006). For this reason, we also show such a comparison in Figure 15. What can be seen is that these observations also show sizable r-process features above the $A = 130$ peak, although they are weaker than in the solar r-element abundances. If such abundance distributions are the result of a single nucleosynthesis pollution, then the “weak” r-process found in the present paper can only marginally explain such features. One could argue, however, that such observed abundance features are a combination of at least two pollution, one (low level) solar r-process and another “weak” r-contribution extending only up to $A = 130$.

5.3. Multi-dimensional Effects

Nucleosynthesis uncertainties due to multi-dimensional effects, i.e., convective turnover, have not been considered here, but we want to discuss their possible impact. Note that convective turnover and the presence of unstable fluid motion are typically associated with compositional mixing, in addition to the ejected material. Their development, e.g., after the shock passage across a low-density environment, can leave peculiar features such as those discussed in Wanajo & Janka (2012) for the example of a 8.8 $M_\odot$ star explosion. In order to give an estimate for our nucleosynthesis results obtained in the presence of possible convection, we evaluated the Ledoux criterion (Wilson & Mayle 1988). It is related to entropy per baryon and lepton-number gradients. We find that regions where these gradients become largely negative, i.e., regions where convection may develop, correspond to either fallback of material or the shock become largely negative, i.e., regions where convection may occur. We find that regions where these gradients prevail (Fischer et al. 2010; Fröhlich et al. 2010). Thus, there seems to exist no chance to produce r-process matter in these innermost regions, despite many interesting parameter studies for NDW ejecta in terms of entropy $S$, electron fraction $Y_e$, and expansion timescale $\tau$ (Hoffman et al. 1997; Meyer & Brown 1997; Freiburghaus et al. 1999a; Farouqi et al. 2010) or hydrodynamic studies, partially with parameter variations (Arcones et al. 2007; Kuroda et al. 2008; Panov & Janka 2009; Roberts et al. 2010; Arcones & Montes 2011). Very recently, Martinez-Pinedo et al. (2012) and Roberts & Reddy (2012), explored charged-current weak processes (i.e., electron-neutrino and anti-neutrino captures on neutrons and protons), consistent with the EOS in neutrino-driven supernova explosion. They find modifications of the reaction $Q$-values due to medium effects, which increase spectral differences between $\nu_e$ and $\bar{\nu}_e$. This results in slightly neutron-rich ejecta. Nevertheless, since the entropy per baryon is still low, a strong r-process is unlikely to occur.

In order to obtain r-process conditions, a better chance to eject neutron-rich matter is provided when neutron-rich matter stems from the initial collapse and compression, where electron captures made it neutron-rich early in an explosion, before neutrino interactions have the chance to turn it proton-rich in the NDW. Core-collapse supernovae, exploding via the quark–hadron phase transition (the focus of the present study), or electron-capture supernovae (Wanajo et al. 2011), which explode without a long phase of accretion onto the proto-neutron star, both lead to a rather prompt ejection of prior

Figure 15. Integrated abundance distributions as a function of atomic charge number $Z$ in comparison to abundance features in “weak r-process” low-metallicity stars as observed by Honda et al. (2006). We also indicate the effect of uncertainties in the $Y_e$ determination, given in terms of percentage $P_{\text{cor}}$.

(A color version of this figure is available in the online journal.)

Nevertheless, this nucleosynthesis site inhabits another possibility of convection due to the explosion mechanism related to the quark–hadron phase transition. It takes place on timescales on the order of several 100 ms, depending on the details of the quark–hadron EOS, in the absence of any other mechanism, e.g., neutrino-driven explosion. On these timescales, large-scale convection may develop before the transition/explosion is initiated. Exploring its impact on the entire explosion and nucleosynthesis scenario will require multi-dimensional simulations, especially related to the point in time when this explosion starts (possibly affected by convection and related neutrino losses and/or uncertainties in the EOS, which both determine the $Y_e$ at the onset of the explosion). This is beyond the scope of the present article and will require future investigation.

6. DISCUSSION AND SUMMARY

 Supernova nucleosynthesis is well understood for the outer ejected mass zones, which can be well approximated by a shock wave with appropriate energy passing through the layers of the progenitor (Woosley & Weaver 1995; Thielemann et al. 1996, 2011; Woosley et al. 2002; Nomoto et al. 2006; Woosley & Heger 2007; Heger & Woosley 2010). What remains uncertain is the composition of the innermost ejecta, directly linked to the explosion mechanism, i.e., the collapse and explosion phase. In the present paper, we analyzed these mass zones of core-collapse supernova explosions triggered by a quark–hadron phase transition during the early post-bounce phase (Sagert et al. 2009; Fischer et al. 2011). A number of aspects are important for understanding these results. The very innermost ejecta are strongly affected by the NDW. Recent investigations noticed that this NDW turns matter proton-rich, producing specific Fe-group isotopes and in the subsequent vp-process nuclei with masses up to $A = 80–90$ (Liebendörfer et al. 2003; Pruet et al. 2005, 2006; Fröhlich et al. 2006a, 2006b; Wanajo 2006). Even in the long-term evolution, proton-rich conditions prevail (Fischer et al. 2010; Hüdepohl et al. 2010). Thus, there seems to exist no chance to produce r-process matter in these innermost regions, despite many interesting parameter studies for NDW ejecta in terms of entropy $S$, electron fraction $Y_e$, and expansion timescale $\tau$ (Hoffman et al. 1997; Meyer & Brown 1997; Freiburghaus et al. 1999a; Farouqi et al. 2010) or hydrodynamic studies, partially with parameter variations (Arcones et al. 2007; Kuroda et al. 2008; Panov & Janka 2009; Roberts et al. 2010; Arcones & Montes 2011). Very recently, Martinez-Pinedo et al. (2012) and Roberts & Reddy (2012), explored charged-current weak processes (i.e., electron-neutrino and anti-neutrino captures on neutrons and protons), consistent with the EOS in neutrino-driven supernova explosion. They find modifications of the reaction $Q$-values due to medium effects, which increase spectral differences between $\nu_e$ and $\bar{\nu}_e$. This results in slightly neutron-rich ejecta. Nevertheless, since the entropy per baryon is still low, a strong r-process is unlikely to occur.

In order to obtain r-process conditions, a better chance to eject neutron-rich matter is provided when neutron-rich matter stems from the initial collapse and compression, where electron captures made it neutron-rich early in an explosion, before neutrino interactions have the chance to turn it proton-rich in the NDW. Core-collapse supernovae, exploding via the quark–hadron phase transition (the focus of the present study), or electron-capture supernovae (Wanajo et al. 2011), which explode without a long phase of accretion onto the proto-neutron star, both lead to a rather prompt ejection of prior
compressed and neutronized matter. However, the \(Y_e\) obtained under such conditions does not support a full \(r\)-process. This kind of outcome also characterizes the conditions we find in the prompt and quasi-prompt ejecta of the present study, which did not experience a strong neutrino flux. However, the \(Y_e\)-values attained are not smaller than 0.33. Whether uncertainties in the input or explosion physics can change this down to values close to 0.23, necessary for obtaining the third \(r\)-process peak, remains to be shown in an upcoming article, where we will include charged-current reaction rates that are consistent with the EOS following Martínez-Pinedo et al. (2012) and Roberts & Reddy (2012).

A related but different phenomenon has been discussed in Jaikumar et al. (2007 and references therein). In their scenario, the quark–hadron phase transition does not happen shortly after core collapse and is not the cause of the supernova explosion. Instead, a regular neutrino-driven supernova explosion occurs first and leads to a deleptonized neutron star with a low-\(Y_e\) and a steep density gradient at the surface. Their scenario of a “quark-novae,” occurring via a quark–hadron phase transition in an existing neutron star, is reported to produce \(r\)-process elements via the prompt ejection of extremely neutron-rich material from the neutron star surface. In this sense, quark-novae differ from the scenario explored in the current study. They result in a more compact object already in \(\beta\)-equilibrium, such that the expansion timescale of the ejected material is much faster than compared to the scenario discussed in the present paper. However, in Jaikumar et al. (2007), the authors apply a very simplified description for the quark–hadron phase transition and ignore neutrino transport in general, as well as weak processes in the hadronic part of their neutron star. The latter may be essential for producing neutrinos that may change \(Y_e\) during shock passage and hence lead to different nucleosynthesis results than what has been discussed in Jaikumar et al. (2007). It remains to be shown if the obtained favorable conditions for the \(r\)-process will remain when applying more sophisticated input physics.

Given our results described above, we conclude that supernova explosions triggered via the quark–hadron phase transition during the early post-bounce phase can contribute to a weak \(r\)-process, consistent with observations of low-metallicity stars (Honda et al. 2006) and with LEPP abundances (Travagl et al. 2004). Such conditions apparently do not occur in regular core-collapse supernovae. However, strong \(r\)-process conditions, which also produce the third \(r\)-process peak and the actinides, have in simulations only materialized in neutron star mergers (Freiburghaus et al. 1999b; Goriely et al. 2011), fast rotating core-collapse supernovae with strong magnetic fields and jet ejecta (Cameron 2003; Nishimura et al. 2006; Fujimoto et al. 2008), or accretion disks around black holes (Surman et al. 2008; Wanajo & Janka 2012). For the explosion model discussed here, an investigation of uncertainties in the hydrodynamics and the nuclear physics input showed that a strong \(r\)-process able to produce up to the third peak elements is rarely possible to obtain.

Neutron star mergers have, in fact, been shown to be powerful sources of \(r\)-process material, ejecting a factor of 100–1000 more \(r\)-process material than required on average from core-collapse supernovae, if those would have to explain solar \(r\)-process abundances. This would actually support the large scatter of Eu/Fe in comparison to, e.g., O, Mg, Si, S, and Ca/Fe, where the latter are clearly produced in supernovae. The only problem is that it might be hard to explain the early appearance of \(r\)-process matter for metallicities at and below [Fe/H] = −3.

Neutron star mergers will appear after the first supernovae have already produced Fe, and studies by Argast et al. (2004) showed that one expects \(r\)-process products only for metallicities [Fe/H] = −3 ∼ −2. Some recent studies that include the fact that our Galaxy is possibly the result of smaller merging subsystems (with different star formation rates) are expected to show a way out of this dilemma. If this cannot be solved, then we need another strong \(r\)-process source already at low metallicities, and it is possible that jets from rotating core collapses with strong magnetic fields could be the solution (see, e.g., Nishimura et al. 2006; Fujimoto et al. 2007; Winteler et al. 2012).

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