Quantitative, real-time, single cell analysis in tissue reveals expression dynamics of neurogenesis

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Short title: Quantitative and dynamic analysis of neurogenesis
Abstract

Despite single cell transcriptomics, how cells make transitions within tissues in real time, is not understood. Here, we use single cell live imaging of an endogenous HES5 reporter and absolute quantification to gain a dynamic view of neurogenesis in the embryonic mammalian spinal cord. We show that HES5 protein expression fluctuates in dividing neural progenitors and becomes more frequently periodic in the transition towards differentiation, creating transient oscillations with higher fold-changes. This dynamic behavior means that the HES5 population heterogeneity observed between cells at a fixed time-point, is a composite of short-term and longer-term dynamics.
Introduction

During embryogenesis cells balance proliferation with differentiation to make cell state transitions that lead to the formation of functional organs. This is exemplified by the development of the central nervous system, which requires the balance of neural progenitor maintenance with differentiation during multiple waves of differentiation into neuronal and glial cell-types. In the dorso-ventral (D-V) axis of the spinal cord, elegant experiments have shown that fate decisions require integration of a wide range of signals over time, many in the form of morphogen gradients, resulting in downstream gene expression changes. Single-cell transcriptomics have greatly enhanced our understanding of these gene expression changes, the gene networks involved in fate decisions and of the bifurcation points where decisions are made.

Transcriptomic studies are powerful in revealing cohorts of up-regulated or down-regulated genes and in defining sub-states and branching points. However, advances in single-cell live imaging of gene expression have shown that it is often highly dynamic, suggesting that the control of cell state transitions is more complex. Rather than being in an “on” or “off” state, a handful of transcription factors have been shown to oscillate with periodicity of a few hours. While such oscillations have been long described in somitogenesis, in the development of neural tissues they are a relatively recent discovery. This is because unlike somitogenesis where oscillations are synchronous within each somite, they tend to be asynchronous in neural cells and so required unstable reporters and single cell imaging to be discovered. Thus, it is not only changes in gene expression levels that are important, but the short term dynamics of gene expression can also carry important information for cell state transitions. Indeed, there is experimental and theoretical evidence that cell fate transitions may be controlled by a change in the dynamic pattern of gene expression, which could be from oscillatory to stable expression, or to oscillatory with different characteristics.

In the case of the transcriptional repressor HES1, a key target of Notch signaling, it has been known that oscillatory expression is driven by transcriptional auto-repression coupled with delays, instability of mRNA and protein and non-linearity of reactions, common principles of many biological oscillators. Like HES1, HES5 is a Notch target bHLH transcription factor (TF) which is highly expressed by neural progenitor cells and decreases in expression as differentiation proceeds. Knock-out mice and over-expression studies have shown that HES5 functions to maintain the undifferentiated progenitor state through repression of proneural genes, such as Neurog2 and Atoh1 that promote neuronal differentiation. Like HES1, HES5 has been shown to oscillate in neural progenitors in vitro.

More recently, it was shown that a change in HES dynamics is mediated by a change of the parameters or initial conditions of the oscillator, most likely represented by a change in mRNA stability or protein translation under the influence of a microRNA, miR-9. Other theoretical studies provide additional support for the importance of a change in dynamics by showing that gene expression networks in the D-V dimension of the spinal cord can generate multi-way switches (stable or oscillatory).
An additional revelation of single-cell live imaging studies is that gene expression is characterised by varying degrees of noise due to the stochastic nature of transcription\textsuperscript{27–29}. Current ideas for the role of such embedded stochasticity include cases where it would be an advantage\textsuperscript{30,31} or conversely, an impediment for cell fate decisions\textsuperscript{32,33} and mechanisms to suppress noise after a fate-decision\textsuperscript{34}.

However, although these studies have shed new light into the problem of cell-state transition, how cells make decision in the context of multicellular tissue is poorly understood. This is because both single-cell transcriptomics and live imaging data are routinely performed in single cells taken out of the tissue environment. Existing studies of oscillatory expression in the mouse brain and spinal cord lack the statistical power needed to give a comprehensive understanding of the dynamics in the tissue\textsuperscript{11,35}. A study using electroporation of a promoter reporter of \textit{Hes5}-1 in chicken spinal cord tissue reported activation of Notch signaling throughout the progenitor cell cycle but most frequently before mitosis\textsuperscript{36}. This approach suffered from plasmid loss and varying degrees of plasmid transfection and did not report on endogenous HES5.

Here, we have taken advantage of a Venus::HES5 knock-in reporter to study the dynamics of HES5 in the context of a tissue, with single cell resolution, over time. We have developed an ex-vivo organotypic slice system of embryonic mouse spinal cord (E10.5) where HES5 dynamics can be continuously imaged over at least 12 hours. We have also developed statistical tools to analyse the behaviour of hundreds of HES5 expressing cells over time. Coupled with absolute quantitation of the HES5 fluorescent fusion protein, we were able to create a finely resolved map that shows precisely the heterogeneity that exists in the tissue and furthermore gives insight into how it is generated.

We report that HES5 expression has a 10-fold range between cells in a single expression domain that can be accounted for by short-term fluctuations and longer-term trends of decreasing HES5. We use hierarchical clustering to define distinct clusters of HES5 expression dynamics and then use cell position and division properties to infer cell state. Surprisingly, we find that most of the oscillatory behaviour is observed in cells that transition towards differentiation where it is coupled with an overall decrease in HES5 expression. By contrast, dividing neural progenitor cells are less frequently periodic but significantly more noisy in their HES5 expression. Computational modelling with stochastic differential delay equations, parameterised using experimental values and Bayesian inference, suggest that in the spinal cord tissue environment the \textit{Hes5} genetic oscillator operates close to a bifurcation point where noise can tip it from aperiodic to periodic expression. Taken together, our findings suggest that single progenitor cells in a tissue environment are “noisy” and are thus primed to enter a transient oscillatory phase as the cells differentiate. Our work reveals for the first time the single-cell dynamics during cell state transitions in a tissue context. Additionally, our study reveals that tissue level single-cell heterogeneity has a complex origin in both short and long term dynamics.
Results

1. Venus::HES5 reporter in the ventral embryonic spinal cord recapitulates endogenous features

We characterised the Venus::HES5 knock-in mouse to ensure that it is a faithful reporter of the un-tagged gene. In transverse sections of the spinal cord at E10.5 Venus::HES5 showed a broad ventral and a smaller dorsal domain (Fig.1a). The ventral domain, which is the focus of this study, encompasses mainly ventral interneuron (p0/p2) and some ventral motorneuron progenitors (p2/pMN) as shown by mapping to appropriate regional (Supp. Fig. 1a and b) and neural/neuronal markers (Sox1/2+ progenitors, NeuN+ neurons, Fig 1b) and consistent with reports of endogenous HES5.

Both mRNA and protein half-lives of Venus::HES5 are unstable with similar values to untagged HES5 (approximately 30 mins for the mRNA and 80-90 mins for the protein). These findings confirm that the Venus::HES5 fusion protein is a faithful reporter of endogenous un-tagged HES5 expression (Supp. Fig.1c-f).

2. Direct imaging and fluorescence correlation spectroscopy (FCS) of Venus::HES5 protein quantifies the range and level of HES5 expression in single cells

Dynamic expression can give rise to tissue level single-cell heterogeneity which may be masked by population averaging on non-quantitative methods. Here, we have imaged nuclear Venus::HES5 intensity directly, to avoid signal amplification associated with immunohistochemistry, and characterised the true heterogeneity in expression within the ventral domain in tissue slices (Fig.1b). We then obtained absolute quantitation of Venus::HES5 molecules at the single cell level by FCS of neural progenitor cells in live homozygous Venus::HES5 E10.5 embryo slices (Fig.1c,d Supp. Fig.2a,b,c). FCS is an absolute quantification method that records fluorescence fluctuations as molecules diffuse through the confocal volume. Therefore, it provides a means of distinguishing true signal from auto-fluorescence and allows for a comparison between different experiments. Single cells showed a 10-fold range of nuclear Venus::HES5 protein expression within the ventral Venus::HES5 expression domain, from 26nM to 319nM. (Fig.1d). The mean Venus::HES5 nuclear concentration was calculated as 140nM, or 46,250 molecules per nucleus. Heterozygous embryos showed lower mean protein expression as could be expected by monitoring the expression of one allele (Supp. Fig.2d) but similar variability between cells. These findings show a high degree of variability in Venus::HES5 expression between cells which is similar in homozygous and heterozygous embryos suggesting that integrating the expression from 2 alleles does not diminish the variability that cells experience.

3. Absolute protein quantitation reveals spatial patterns of single-cell heterogeneity throughout the HES5 expression domain

FCS can be performed for a limited number of live cells in the tissue, while an intensity map based on the Venus signal can be obtained for all cells from snapshot images. By combining the two approaches we were able to obtain a quantitative map
of all expressing cells along the D/V axis of the spinal cord\textsuperscript{38}. We plotted the distribution of single-cell Venus::HES5 intensities from manual segmentation of nuclei in a single slice (Fig.1g) against the distribution of single-cell FCS protein concentration (Fig.1h) over multiple slices and experiments. The resulting quantile-quantile (Q-Q) plot is linear and only deviates from linearity at the very high and low values (Fig.1i). Therefore we can turn intensity in an image into protein concentration (Fig.1j) by scaling the intensity value by the gradient of the linear Q-Q plot. Once the Venus::HES5 protein concentration distribution has been obtained by FCS it can be applied to multiple images to generate more quantitative maps without the need to repeat the FCS (see Supp. Fig. 2e for another example).

We then used this quantitative map to look at the global and local pattern of HES5 concentration. We split the ventral domain into 2 regions due to the difference in the width of the ventricular zone along the D-V axis (as indicated by boxes in Fig.1j) We observed a non-linear global reduction of Venus::HES5 concentration with increasing distance from the ventricle (Fig. 1k). The shoulder-point corresponded to around 50µm and 30µm in the dorsal-most (1) and ventral-most (2) regions respectively, suggesting that at this distance, cells start to decrease HES5. At any given distance there is a large degree of cell-to-cell variability in Venus::HES5 concentration. For example, within the first 20µm (roughly 2 nuclei lengths) of the ventricular zone in region 1, some cells have as low as 130nM of Venus::HES5 while others have as high as 250 nM of HES5 expression, a 1.9-fold difference. The concentration difference between a cell and its nearest neighbour (Supp. Fig.2f) increased further away from the ventricle, reaching a maximum of 191nM, a 4.5-fold difference (Fig. 1l). This trend was confirmed in embryos that had not undergone intensity:concentration scaling (Fig.1m). Thus, a global reduction of Venus::HES5 expression further from the ventricle is accompanied by a high degree of fine-grained heterogeneity that increases with increasing distance from the ventricle.

4. Hierarchical clustering reveals distinct Venus::HES5 expression dynamics

Single cell expression heterogeneity, as described above, may be the result of multiple possibilities: i) fluctuating expression alone (Fig.2ai), which could be periodic and asynchronous ii) distinct but stable cell-state subpopulations (Fig.2a(ii)) or iii) an expression decline as cells transition from one stable state to another (Fig.2a(iii)). Hypothesis (i) implies HES5 dynamic expression satisfies ergodicity, i.e. variability in a single cell over time can recapitulate the tissue level heterogeneity\textsuperscript{39}. To resolve these possibilities for the first time, we performed live imaging of Venus::HES5 expression dynamics at single cell level, in the tissue context of ex-vivo slices in Sox1+ neural progenitor cells (Fig. 2b,c).

We observed multiple types of single-cell Venus::HES5 dynamic behaviours in heterozygous neural progenitor cells (Fig. 2d) over a time period of 12-15 hours. Hierarchical clustering of the standardised Venus::HES5 intensity timeseries suggested 4 clusters of different types of long-term Venus::HES5 expression dynamics (Fig.2e and Supp. Fig. 5). Cells in cluster 1 and 2 show fluctuating expression around a stable mean whereas cells in clusters 3 and 4 show gradually decreasing and fluctuating HES5 expression (Fig. 2e). The non-standardised mean
expression of cells in each cluster maintain this trend (Fig.2f) which is further exemplified by single cell traces (Fig.2g).

The coefficient of variation (C.O.V) of Venus::HES5 over time in single neural progenitor cells (standard deviation of intensity divided by the mean intensity) increased when cells were tracked over 4,8,12,14.25 and 17.25 hours (Fig.2h). By 8-12 hours multiple cells in clusters 3 and 4 had reached similar or higher levels of variation as the variation observed between cells at a single snapshot (Fig.2h) suggesting that declining expression is a major contributor to the tissue heterogeneity. In contrast, cells in clusters 1 and 2 rarely, if ever, reached tissue-levels of variation between cells at a single point in time, suggesting that short-term dynamics have a lesser contribution to overall tissue heterogeneity (and excluding scenario i).

Thus, there exists a limited number of HES5 expression dynamics in neural progenitor cells, represented by clusters, and heterogeneity is generated by a mix of declining expression (long-term trends, scenario Fig.2a iii,) and dynamic fluctuations (short term dynamics, scenario Fig.2a ii,) around a slowly varying mean.

5. Distinct patterns of Venus::HES5 expression dynamics correlate with cell-states and decision processes.

We hypothesise that the different clusters of Venus::HES5 expression, revealed by hierarchical clustering, may represent different cell-states present in the Sox1+ progenitor population. It is well known that proliferating neural progenitors (Sox1+/2+) are found apically in the ventricular zone, undergo inter-kinetic nuclear migration (INM) and divide at the apical surface of the ventricle\(^1,40\). Newly born cells fated towards neuronal differentiation migrate basally away from the apical surface in to the mantle zone and exit the cell cycle, turning on markers of differentiation (Tuj1 and NeuN)\(^40\). We therefore sought to infer the cell state by position, motility and division, recorded from individually tracked nuclei with the ventricle as a reference point. Fig.3a and Supp. Movie 1 show an example track for each cluster and Fig.3b all clustered cells from 1 experiment.

The average position of cells in cluster 1 was significantly closer to the ventricle than those in cluster 3 (Fig.3c). However, the main difference between the positions of the clusters is evident in a zone greater than 50µm from the ventricle, where very few cells of cluster 1 reside and cells in cluster 3 are more abundant (Fig.3d). By contrast, the zone within the first 50µm of the ventricle is equally occupied by cells in clusters 1-4 (Fig.3d).

Nuclei of cells in cluster 1 moved both apically and basally, consistent with inter-kinetic nuclear migration (INM) but had the shortest displacement as they returned to the ventricular zone. Meanwhile nuclei of cells in cluster 3 and 4 had a larger displacement which was unidirectional towards the basal side (Fig. 3a,b,e,f and Supp. Fig.7a). The average position of nuclei in cluster 3 tends to be located further away from the ventricle, suggesting they are on their way to differentiation (Fig.3c and Supp. Fig.7a). Measurement of the size and position of the Sox2+ domain by immunostaining of slice cultures showed that many cells in cluster 3 and 4 moved out
from the Sox2+ zone into the mantle zone with concurrent decreasing Venus::HES5 (Fig.3a,b, Supp. Fig.7a,b,c). In addition, the percentage of cells that divided in the 12-hour monitoring window was significantly higher in cluster 1 and 2; indeed, very few cells in cluster 3 or 4, (if any) were observed to divide (Fig.3g). Given these findings, we inferred that cells in cluster 1 and 2 are proliferating progenitors and cells in cluster 3 and 4 are transitioning towards differentiation.

We confirmed our interpretation of cell-state based on cellular behaviour by treating the spinal cord slice cultures with the Notch inhibitor DBZ to promote differentiation. Spinal cord slice tissue treated with 2µM DBZ showed significantly lower mean Venus::HES5 intensity than control DMSO treated slices (Fig.3h, Supp.Fig. 7d) and an increase in the early neuronal marker B3-tubulin especially in apical regions (Fig.3i). The disorganisation of the neural tube in DBZ treated slices is similar to Hes KO phenotypes. The average position of single cells in DBZ treated slices was further from the ventricle (Supp. Fig. 7e) and they showed significantly increased apico-basal displacement confirming that the Notch inhibition had pushed cells towards basal migration and differentiation (Fig.3j). Hierarchical clustering of standardised Venus::HES5 single-cell intensities showed that 98% of cells in the DBZ treated slices were found in clusters 3 and 4 (Fig. 3k,l) while the distribution of DMSO Venus::HES5 cells recapitulated the presence of all 4 clusters (Supp. Fig.7f,g).

We conclude that cells characterised by a temporally fluctuating Venus::HES5 expression pattern around a high mean (cluster 1 and 2) are proliferating neural progenitors maintained by Notch signalling, while cells with decreasing Venus::HES5 levels over time (clusters 3 and 4) are non-dividing progenitors undergoing cell state transition to differentiation.

6. Cells undergoing state transition to neurons are more frequently oscillatory while proliferative progenitors are more noisy

HES5 expression has been reported to be periodic in proliferating mouse neural stem cells derived from the embryonic cortex. Therefore we sought to determine whether any of the clusters showed oscillatory expression. HES5 traces show a high degree of variability in period and amplitude. Detecting oscillatory gene expression in such noisy timeseries, is very challenging and we have previously developed a statistical approach for noisy bioluminescent data, whereby single cell periodicity can be inferred and a statistical confidence level is imposed at population level. Here, we have developed an extension of this method to take into account that fluorescence intensity timeseries from tissue are inherently more noisy (Supp. Methods A). Further, we introduced robust procedures by which globally-informed priors are used to facilitate parameter inference from short timeseries (see Supp. Methods A).

To analyse oscillations, we first corrected for long-term changes in level (trend) caused by HES5 downregulation (Fig. 4a). We then analysed the detrended data with an oscillatory covariance model and inferred the period, amplitude and lengthscale (Fig. 4b). The first two parameters characterise the overall behaviour of the oscillator while the latter accounts for variability in the peaks over time. We
compared the oscillatory (alternative) model fit with that obtained from an aperiodic (null) covariance model fit using the log-likelihood ratio (LLR) statistic, which is high for oscillators (Supp. Fig.8b) and low for non-oscillators (Supp. Fig. 8c). Finally, we identified oscillatory cells in each experiment using a strict false-discovery rate criteria set at 3% (Supp. Fig.8e).

We found that overall only 47% of cells showed oscillatory Venus::HES5 expression dynamics (Supp. Fig.8a), while the rest were fluctuating and aperiodic. The estimated period of Venus::HES5 oscillations showed a distribution with a mean of 3.3±0.3 hours (Fig.4d) while H2B::mCherry expression from the ROSA26 locus collected from the same nuclei was aperiodic (Supp. Fig.8a). Surprisingly, oscillations were not restricted to proliferating progenitor cells. Instead, there was a tendency for more progenitor cells on their way to differentiation (clusters 3 and 4) to pass oscillatory tests than dividing progenitors in clusters 1 and 2 (Fig.4c). By contrast, proliferating progenitors in cluster 1 had significantly greater noise than differentiating cells in cluster 3, (more cells with a higher squared-standard deviation of the de-trended Venus::HES5 signal (Fig.4e)). In agreement with this, the likelihood of a cell to have oscillatory Venus::HES5 significantly increased with an increasing average distance from the ventricle (Fig. 4f), whereas noise decreased (Fig.4g).

Given that progenitor cells close to the ventricle (cluster 1 & 2) must turn into the transitory and differentiating cells in cluster 3 and 4, we conclude that progenitor cells have high, dynamic and noisy Venus::HES5 expression which evolves in to a more oscillatory signal as Venus::HES5 decreases and the cells undergo differentiation. Although our observational time window is relatively short, data collected from a few cells in cluster 1 demonstrate this noisy to oscillatory transition in Venus::HES5 expression, supporting this view (Fig.4h, Supp.Fig.9a, Supp. Movie 2).

7. Mathematical modelling shows the Hes5 oscillator is poised at aperiodic to oscillatory transition.

To understand how the HES5 dynamics of clusters 1 and 2 are generated and how they may transition from aperiodic to periodic expression, we used a stochastic delay differential equation model of an auto-negative feedback network (Fig.5a and Supp. Methods B)\(^{30,43-45}\). We parameterized the model using protein and mRNA half-lives (Supp.Fig.1c,d) and Approximate Bayesian Computation (ABC)\(^{46}\) to infer parameters that are not directly experimentally known (see Supp. Methods B). ABC has advantages over commonly-used point estimates because it provides a probability distribution for estimated parameters thus quantifying parameter uncertainty. We used ABC to search for parameters that give rise to experimentally observed summary statistics of HES5 expression (see Supp. Methods B) and we found that the experimentally measured distribution of oscillation periods and relative standard deviation values in clusters 1 and 2 (Supp. Fig. 10a and Supp. Fig. 10b respectively) are consistent with the predictions from these parameters (Fig. 5b,c).

HES5 expression simulated from inferred parameters can be aperiodic (Fig.5di) or oscillatory (Fig. 5dii,iii) depending on the parameters, as illustrated qualitatively by a sharpening of the peak in the power spectrum and expressed quantitatively by coherence\(^{30}\) (Supp. Methods B). At unique combinations of parameter values the
stochastic model can generate different proportions of aperiodic and oscillatory HES5 expression, across traces and within the same trace. This is consistent with our experimental observations where less than half of cells pass oscillatory tests and we can observe changes in expression dynamics.

We investigated how HES5 expression may transition from aperiodic to oscillatory in two steps. Firstly, we investigated how oscillation coherence varies in response to a single parameter change, in this case the protein degradation rate across parameter space using Bayesian inference (Fig. 5e where each curve corresponds to one possible parameter combination). The experimentally measured protein degradation rate (protein half-life of 90 minutes, blue-line Fig. 5e) defines a transition point where the range of possible coherence values changes sharply.

Secondly, we determined the expected coherence in relation to the protein and mRNA degradation rates for the full stochastic model (Fig. 5f) and the deterministic model (Fig. 5g). The experimentally measured mRNA and protein degradation rates were located in a region of parameter space where oscillations are expected in the stochastic model, but not in the deterministic model. This is consistent with the results of a full Bayesian comparison between the stochastic and deterministic model (Supp. Methods B) where the likelihood of the deterministic model to describe the HES5 expression statistics is more than 160 times smaller than that of the stochastic model (Supp. Fig. 10d). Oscillations were observed in the stochastic system and our experimentally measured degradation rates placed the stochastic system at the boundary of high and low coherence.

Taken together, our modelling suggests that the HES5 oscillator in spinal cord neural progenitor cells is enabled by noise\(^{30,47}\) and operates very close to the boundary between aperiodic and oscillatory model dynamics, where small parameter changes can cause a transition between non-oscillatory (low coherence) and oscillatory (high coherence) expression.

**8. Oscillations on a downward trend increase the fold-changes experienced by target genes**

Detecting oscillations in differentiating cells (cluster 3 and 4) was unexpected based on previous studies. To understand the significance of this finding, we have characterised the dynamic of cells in cluster 3 and 4 in greater detail. We used the Hilbert transform technique for reconstructing instantaneous amplitude (Fig 6a and Supp. Fig 8g) and instantaneous phase (Supp. Fig. 8h) from detrended data. Phase information was used to identify peaks and troughs in the signal to extract fold changes in amplitude (see Supplementary Methods A).

The gradual decrease in mean Venus::HES5 expression in cluster 3 and 4 cells is accompanied by decreasing amplitude of oscillations over time (Fig. 6a, b and Supp. Fig 8g) suggesting that Venus::HES5 undergoes amplitude death as the expression is terminated, while the period of oscillators appears to be unaffected (Supp. Fig. 8h). Surprisingly, although amplitude decreases with differentiation, the maximal peak-to-trough fold change in Venus::HES5 expression in single cells was significantly higher
in differentiating cells in clusters 3 and 4 than proliferating progenitors in cluster 1 (Fig.6c). Furthermore, within cluster 3, oscillatory cells have a higher mean peak-to-trough fold change than aperiodically fluctuating cells (Fig.6d,e). Taken together, these findings suggest that oscillations on top of a long-term decreasing signal transiently promote larger fold-changes and thus, may impart greater changes in HES5 molecule number to downstream target genes than either one alone.

Discussion

In this paper, we have investigated how individual Sox1+ neural progenitor cells make cell state transitions in the multi-cellular environment of the embryonic spinal cord. We have also developed statistical tools and computational models to analyse and interpret stochastic dynamics. Our main findings are twofold: firstly, we found that oscillatory expression of HES5 with a periodicity of a few hours is observed in neural progenitor cells in their native tissue environment and occurs more frequently and with higher fold change in cells that are in transition to a differentiated state (Fig. 6f). Secondly, we show that cell-to-cell heterogeneity in HES5 at the tissue level is a composite of long term dynamics (decline in expression) and short term dynamics (fluctuations in a short time scale), the contribution of each was precisely identified using absolute protein quantification.

The first finding supports the existing hypothesis that HES5 oscillates in neural progenitor cells and that HES5 expression declines as cells differentiate. These findings support the view that changes in expression dynamics correlate with transitions in cell state. However, contrary to expectations, we show that only about 30-40% of the dividing progenitors located close to the ventricle show oscillations that pass a statistical test we developed for stochastic oscillators. Our findings also contrast with the current view that only neural progenitors show gene expression oscillations. Instead, we have uncovered a previously unknown state in progenitor cells further away from the ventricle, transitional to differentiation, where oscillations tend to be more frequently observed. By contrast, dividing progenitors that are closer to the ventricle, have a higher level of HES5 expression noise and have a higher proportion of cells that show aperiodic fluctuations. Therefore we observe both oscillatory and non-oscillatory dynamics within 2 defined sub-states – proliferative progenitors and transitional differentiating cells, with the oscillatory dynamics being more likely in differentiating cells.

Computational modelling helped to determine how the dynamics of HES5 expression are generated. A stochastic model of genetic auto-repression recapitulates statistics of the experimentally measured period and maximum amplitude of HES5 protein expression and indicated that HES5 oscillations are enabled by stochastic amplification. According to our mathematical modelling, the HES5 auto-repression network operates near a bifurcation boundary where small changes in parameter values, such as protein degradation rate, can cause cells to switch between aperiodic and periodic expression. Thus the stochastic dynamical model of HES5 supports the existence of transitions between oscillatory and non-oscillatory regimes in the same cells.
In our modeling, we have included the effects of intrinsic stochastic noise, since this choice of noise does not introduce further model parameters and it is inevitably associated with any rate process. Phillips et al. suggested that the low HES1 molecule number leads to stochastic oscillations of HES1 through a finite number effect. By contrast, HES5 molecule number is not low, (approximately 40-60k molecules per nucleus for HES5 versus while 2-3K per nucleus for HES1\(^3\))). Thus other sources of noise may need to be considered. We hypothesise that noise from stochastic activation of Notch cell-cell signalling in the densely packed tissue as cells undergo INM may actually interfere with the periodicity and coherence of HES5 oscillatory dynamics. An alternative and not mutually exclusive possibility is that additional noise is introduced by cell division\(^4\) or the cell cycle, which would fit our observation that dividing progenitors of cluster 1 have the highest proportion of noisy cells. While there is a view that noise is an undesirable feature of biological systems that needs to be mitigated, there are several cases where noise and the stochasticity that derives from it, may in fact carry some benefit to the decision making process\(^3\). In the case reported here, the benefit of noise may be to "prime" HES5 expression such that it is poised to become oscillatory.

What is the impact of HES5 periodic and/or aperiodic fluctuations on the control of neurogenesis? The HES5 oscillator operates around a high mean with low peak-to-trough amplitude in dividing progenitor cells and it is unclear whether such low amplitude noisy oscillations of HES5 have a role beyond a priming function. The small differences in peak and trough levels may be difficult to differentially decode by downstream genes. Most likely, these oscillations are a by-product of an "active" negative feedback loop that is required for maintaining the HES5 level around a high mean, thus repressing pro-neural genes in most apical progenitors. By contrast, oscillations in the transition to differentiation are coupled with an overall declining trend, and thus generate larger fold differences, which may be easier for downstream targets to decode. This is analogous to a ball bouncing down steps and undergoing greater height drops (oscillatory expression) than a ball rolling down a ramp (aperiodic expression). Since HES proteins are transcriptional repressors for pro-neural genes, such as Neurog2 and Atoh1\(^21,49\) we predict that the larger fold-changes generated by oscillatory decline in HES5 induces an oscillatory onset of downstream proneural genes\(^11,35\). We would argue that coupling HES5 oscillations with a declining trend is an ingenious biological way for the cells to be able to decode what is normally a very shallow HES5 oscillator and importantly, to couple it with the process of differentiation.

The second main contribution of this paper is to increase the depth of our understanding of the degree and origin of cellular heterogeneity in gene expression in a tissue environment. While heterogeneity is a common emerging theme during mammalian development, it’s origins remains poorly understood. We conclude that HES5 expression in the spinal cord is not an ergodic system since tissue level variability cannot be explained from short-term single cell variability but through a combination of cell sub-states co-existing in the tissue (which can be resolved spatially and dynamically) and transitions between these sub-states. Specifically, hierarchical clustering identified 4 clusters based on their short term and long term
dynamics. We have found that a progenitor zone close to the ventricle (<50µm) shows maximum heterogeneity in cell-states, as all 4 dynamic expression clusters are equally represented in this zone, but minimum cell-to-cell heterogeneity in HES5 expression levels. By contrast, in the progenitor zone further from the ventricle there is minimum heterogeneity in cell-states, as it occupied mainly by cells in clusters 3 and 4, and maximum cell-to-cell heterogeneity in HES5 expression levels, approaching a 10-fold range in HES5. Furthermore, single cells undergoing differentiation start to down-regulate Venus::HES5 at any point between 20-50µms away from the ventricle indicating that cells can make the cell fate decision at any point along the apical-basal dimension of the progenitor zone. This contrasts with the widespread schematic view that cell fate is controlled deterministically at global tissue level through signalling gradients. Instead we find that progenitor cells make stochastic fate decisions through a complex and yet unresolved integration between global and local cell-cell signalling.

Our findings highlight the importance of integrating gene expression dynamics with spatio-temporal cell behavior to understand cell state transitions in real time in a multicellular tissue. Challenges for the future include understanding the local spatial cell-to-cell pattern in HES5 expression and extending this type of analysis to observing the expression dynamics of several genes simultaneously, for which a step change in live imaging capabilities/image analysis will be needed.

**Materials and Methods**

**Animal models**

Animal experiments were performed under UK Home Office project licenses (PPL70/8858) within the conditions of the Animal (Scientific Procedures) Act 1986. Animals were only handled by personal license holders. Venus::HES5 knock-in mice (ICR.Cg-Hes5<tm1(venus)Imayo>) was obtained from Riken Biological Resource Centre, Japan and maintained as a homozygous line. In these mice the mVenus fluorescent protein is fused to the N-terminus of endogenous HES5. Sox1Cre:ERT2 mice (Sox1tm3(cre/ERT2) were obtained from James Briscoe with the permission of Robin Lovell-Badge. R26R-H2B::mCherry mice were obtained as frozen embryos from Riken Centre for Life Science Technologies, Japan and C57Bl6 mice were used as surrogates. Sox1Cre:ERT2 and R26R-H2B::mCherry were crossed to generate a double transgenic line homozygous for R26R-H2B::mCherry and heterozygous for Sox1Cre:ERT2.

**Embryo slicing**

Homzygous Venus::HES5 knock-in females were mated with R26R-H2B::mCherry Sox1Cre:ERT2 males and E0.5 was considered as midday on the day a plug was detected. Intra-peritoneal injection of pregnant females with 2.5 mg Tamoxifen (Sigma) was performed 18 hours prior to embryo dissection. Whole embryos were screened for H2B::mCherry expression using Fluar 10x/0.5 objective on a Zeiss LSM880 confocal microscope and the trunks of positive embryos were embedded in 4% low-gelling temperature agarose (Sigma) containing 5mg/ml glucose (Sigma).
200µm transverse slices of the trunk around the forelimb region were obtained with the Leica VT1000S vibratome and released from the agarose. Embryo and slice manipulation was performed in phenol-red free L-15 media (ThermoFisher Scientific) on ice and the vibratome slicing was performed in chilled 1xPBS (ThermoFisher Scientific).

**Fluorescence Correlation Spectroscopy (FCS)**

E10.5 transverse spinal cord slices heterozygous or homozygous for Venus::HES5 were stained on ice for 1.5 hours with 50µM Draq5 (ThermoFisher Scientific) diluted in phenol-red free L-15 (ThermoFisher Scientific) media. FCS experiments and snapshot images of whole spinal cord were carried out using a Zeiss LSM880 microscope with a C-Apochromat 40x 1.2 NA water objective on slices placed directly on a glass-bottomed dish (Greiner BioOne) kept at 37°C and 5%CO₂. FCS signals were collected inside single nuclei in either the ventral region alone or both dorsal and ventral regions for tissue experiments. Venus (EYFP) fluorescence was excited with 514 nm laser light and emission collected between 517 and 570nm. Data from individual cell nuclei was collected using 5 x 2 s runs at 0.15 to 0.3% laser power which gave <10% bleaching and a suitable count rate ~1 kHz counts per molecule (CPM). To obtain molecule number, autocorrelation curves were fit to a two-component diffusion model with triplet state using the Levenberg-Marquardt algorithm in MATLAB optimization toolbox with initial conditions assuming a ‘fast’ diffusion component 10x faster than the ‘slow’ component as previously described. Measurements collected from cells exhibiting large spikes/drops in count rate or with low CPM (<0.5 kHz), high triplet state (>50%), or high bleaching (>10%) were excluded from the final results. Number and brightness analysis of the count rate showed a high correlation with molecule number obtained from autocorrelation curve fitting. The effective confocal volume had been previously determined with mean 0.57fL ± 11 fL (S.D.) allowing conversion from molecule number to concentration. Single-cell data of number of molecules in the cell nucleus was obtained by adjusting concentration to the average volumetric ratio between nuclear volume and confocal volume. Mean nuclear volume of 523 fL was estimated using H2BmCherry intensity and 3D reconstruction from z-stack images in Imaris (Bitplane).

**Generating a quantitative expression map**

Individual Draq5+ nuclei in a tile-scan image of a transverse slice of the whole E10.5 spinal cord were manually segmented as ellipses using ImageJ and the Venus background intensity subtracted. A quantile-quantile plot was generated for the distribution of nuclear Venus::HES5 intensities from manual segmentation of a single image and the distribution of nuclear Venus::HES5 concentrations from FCS of cells throughout the E10.5 spinal cord from multiple slices and experiments. Linear regression was used to generate a calibration curve between Venus::HES5 intensity and Venus::HES5 concentration over the middle 90% of the range. The gradient of the line was used as a scaling factor and applied to the pixel intensity values in the segmented image to transform intensity to concentration.

**Analysis of variability in Venus::HES5 in snapshot images**
The centroids of the manually segmented cells from a quantitative expression map were used to measure distance from the ventricle and perpendicular to the D/V axis. Neighbours were ranked based on distance from the centroid of the cell of interest and the nearest neighbours were classified as the cells in the first rank (Supp. Fig. 2f). Coefficient of variation of Venus::HES5 intensity was measured by manual segmentation of Draq-5 stained transverse slices of whole E10.5 spinal cord in ImageJ.

**Embryo slice culture and live imaging**

E10.5 spinal cord slices for live time lapse microscopy were placed on a 12mm Millicell cell culture insert (Merck Millipore) in a 35mm glass-bottomed dish (Greiner BioOne) incubated at 37°C and 5%CO₂. The length of the legs of the cell culture insert were reduced to decrease the distance from the glass to the tissue. 1.5mls of DMEM F-12 (ThermoFisher Scientific) media containing 4.5mg/ml glucose, 1x MEM nonessential amino acids (ThermoFisher Scientific), 120ug/ml Bovine Album Fraction V (ThermoFisher Scientific), 55µM 2-mercaptoethanol, 1x GlutaMAX (ThermoFisher Scientific), 0.5x B27 and 0.5x N2 was added. Movies were acquired using Zeiss LSM880 microscope and GaAsP detectors with a Plan-Apochromat 20x 0.8 NA objective with a pinhole of 5AU over a z-stack of roughly 70 um every 15 mins for 18-20 hours. DMSO or 2µM DBZ (Tocris) was added to media immediately before imaging.

**Image analysis and cell tracking**

Briefly, single cells were tracked using the H2B::mCherry channel. Single-cell Venus and mCherry expression were normalised to the whole tissue mean for the relevant channel to account for any possible photobleaching. For hierarchical clustering single-cell Venus::HES5 expression from 12-hour tracks was standardized by subtracting the mean and dividing by the standard deviation of the single-cell signal.

Single neural progenitor cells in E10.5 spinal cord slices were tracked in Imaris on the H2BmCherry channel using the ‘Spots’ and ‘Track over time’ function. Spot detection algorithm used background subtraction and tracking used the Brownian motion algorithm. All tracks were manually curated to ensure accurate single-cell tracking. A reference frame was applied to the movie along the dorso-ventral and apico-basal axes of the spinal cord to allow the distance from the ventricle to be calculated. To account for any photobleaching and allow comparison of intensities between movies the mean intensity of mCherry and Venus in each spot was normalised to the mean intensity of mCherry or Venus in the whole tissue. The whole tissue volume was tracked using the ‘Surfaces’ and ‘Track over time’ function.

There was no correlation in Venus::HES5 and H2BmCherry expression suggesting the Venus::HES5 dynamics were not a result of global changes in transcription or translation in the cell or microscope anomalies (Supp. Fig 3a-d and further examples in Supp. Fig. 6). We also investigated the relationship between Venus::HES5 and z-position in the tissue (Supp Fig. 4a-d). As expected from imaging through tissue there was a small negative correlation (r = -0.24) between Venus::HES5 intensity and z-position when all cells and time-points were plotted (Supp. Fig. 4b). However the
range of z-positions in a single cell 12-hour track was rarely greater than 25µm, therefore it is unlikely the fluctuations and oscillations in Venus::HES5 are a result in changes in z-position (Supp. Fig. 4c). Further at the single-cell level there is no difference in the correlation coefficient between z-position and Venus::HES5 intensity when comparing oscillatory and non-oscillatory cells (Supp. Fig. 4d).

Hierarchical clustering

Prior to analysis, timeseries of single cell Venus::HES5 expression were normalised to tissue mean to account for bleaching per independent experiment and in addition standardised (z-score calculation) by subtracting the mean of the timeseries from each timepoint and dividing by the standard deviation of the timeseries. Standardising the data enables clustering on relative expression changes rather than absolute expression levels. Standardised single cell timeseries were then subject to hierarchical clustering using Euclidean distance and Ward’s linkage in RStudio (R Project). Experiments were clustered separately and each clustergram independently identified 4 clusters per experiment. The elbow method to look at the variance explained as a function of number of clusters (nbclust package, R), suggested 4-6 clusters as the optimal cluster number however 5 and 6 clusters were not favoured by silhouette method (nbclust package, R) so we chose 4 clusters (data not shown). Cluster relationships varied between experiments thus for annotation between experiments corresponding clusters labels were determined by calculating average single-cell coefficient of variation (COV) in Venus::HES5 over time for each cluster and comparing to results of clustering experiment 1 (Supp. Fig. 5b). Thus, four clusters with the same COV profile are reproducibly identified in each experiment.

For DBZ-treated cells, data could not be corrected for photobleaching since Venus::HES5 downregulation is induced at tissue level causing a significant drop in tissue mean and masking effects from bleaching. Prior to analysis both DMSO and DBZ timeseries were standardised by z-scoring. To enable comparison between DBZ-treated and negative control DMSO-treated cells, experimental data from both treatment conditions were clustered together (Fig. 3k) as well as clustering DMSO independently of DBZ (Supp. Fig. 7) yielding similar cluster profiles to untreated cells (Supp. Fig. 5a).

Venus::HES5 expression analysis – long trends

For 4, 8, 12, 14.25 and 17.25 hour time windows the coefficient of variation (standard deviation/mean x100) of all the normalised Venus::HES5 intensity values for a single cell in the time window was calculated. The shoulder point of Venus::HES5 was defined as a turning point in the signal that lead to a decrease of greater than 50% of the signal.

Detection and analysis of oscillations – short term dynamics

We analysed oscillations in the HES5 timeseries using the Gaussian Processes approach in Phillips et al. Data was de-trended to remove long term behaviour such as down-regulation and to recover the oscillatory signal with zero mean (see Supplementary Methods Section A). We used maximum likelihood estimation to fit the de-trended data timeseries with two competing models: a fluctuating aperiodic
one (null model) and an oscillatory one (alternative model). We used the log-likelihood ratio statistic to compare the likelihood of data being oscillatory or non-oscillatory and determined the oscillators based on a false discovery rate of 3% independently per experiment. Additional procedures for dynamic parameter inference were introduced and are detailed in Supplementary Methods Section A (see also Supp. Fig. 8d,f).

**Fold change detection in signal amplitude**

We used an unsupervised technique of amplitude reconstruction based on the Hilbert transform. This allows us to robustly identify peaks and troughs in noisy timeseries and compute fold changes as peak-to-trough variations in the signal containing the long term trend. This procedure is described in Supplementary Methods.

**Stochastic model of genetic auto-repression**

We model protein expression dynamics emerging from genetic autorepression and transcriptional delay using an established mathematical model\(^45\). This model includes the effects of transcription and translation as well as degradation of protein and mRNA. We adjust the model to include noise due to intrinsic stochasticity\(^43,55\). We parameterized the model using the experimentally measured mRNA and protein half-lives (30 and 90 mins respectively, Supp. Fig.1c,d,e,f) and approximate Bayesian computation (ABC)\(^46,56\) (Supp.Fig.10c,d,e, Table 1) to search for parameter combinations which modelled a mean HES5 expression of 55000-65000 protein molecules (Supp.Fig.10a) and standard deviation over time of greater than 5% (Supp.Fig.10b). ABC provides probability distributions of model parameters given experimentally observed data; ABC is a standard method for parameterising stochastic mathematical models. We limit the parameter inference to biophysically realistic parameter ranges (Supp.Table 1&2). Details of the model implementation and parameter inference are available in the supplementary methods (Supplementary Methods B).

**Statistical testing**

Statistical tests were performed in GraphPad Prism 7. Data was tested for normality with D’Agostino-Pearson test. The relevant parametric or non-parametric test was then performed. If necessary outlier removal was performed using ROUT method (GraphPad). Coefficient of variation is defined as standard deviation (SD) over the mean.

Bar plots (simple or stacked) and discrete scatter plots show mean or mean±SD where multiple independent experiments are analysed. Statistical significance between 2 datasets was tested with either Student t-test (parametric) or Mann-Whitney test (non-parametric). Statistical significance (p<0.05) for 2+ datasets was tested by Kruskall-Wallis with Dunn’s multiple comparison correction. All tests were 2-sided. Multiple comparison testing involved comparing all pairs of data columns. Correlations were analysed using Spearman rank correlation coefficient. Sample sizes, experiment numbers, p values<0.05 and correlation coefficients are reported in each figure legend.
**Immunofluorescent staining**

Trunks of E10.5 embryos for cryo-sectioning were fixed in 4% PFA for 1 hour at 4°C, followed by 3 quick washes with 1xPBS and 1 longer wash for 1 hour at 4°C. Embryos were equilibrated overnight in 30% sucrose (Sigma) at 4°C before mounting in Tissue-Tek OCT (Sakura) in cryomoulds and freezing at -80°C. 12µm sections were cut on Leica CM3050S cryostat. E10.5 spinal cord slices cultured on Millicell inserts were fixed in 4% PFA for 4 hours. For staining, tissue and sections were washed in PBS followed by permeabilisation in PBS 0.2% Triton X-100 (Sigma) and blocking with PBS 0.05% Tween20 (Sigma) + 5% BSA (Sigma). Primary and secondary antibodies were diluted in PBS 0.05% Tween20 + 5% BSA. Tissue was incubated with primary antibodies overnight at 4°C, then washed three times for 5–10 minutes in PBS 0.05% Tween20, incubated with secondary antibodies and DAPI (Sigma) for 4 hours at room temperature, and washed again three times in PBS-T. Sections were mounted using mowiol 4-88 (Sigma).

**Primary antibodies used were**
- rabbit anti-SOX2 (ab97959, 1:200)
- mouse anti-NeuN (Merck MAB377, 1:100)
- mouse anti-NKX2.2 (74.5A5, Developmental Studies Hybridoma Bank, 1:10)
- mouse anti-PAX7 (Developmental Studies Hybridoma Bank, 1:10)
- rabbit anti-β3-tubulin (Cell Signaling Technology, 5568S 1:200).

**Half-life experiments**

Primary NS cells were isolated from dissected spinal cords of E10.5-11.5 embryos from Venus::HES5 knock-in mice and cultured as previously described. NS-E cells were a gift from Jennifer Nichols (Cambridge Stem Cell Institute, UK). Protein half-life was obtained by transfection of 3xFlag-HES5 and 3xFlag-Venus::HES5 in to NS-E cells with Lipofectamine 3000 (ThermoFisher Scientific) as per manufacturers’ instructions. 24 hours after transfection, cells were treated with 10µM cycloheximide (Sigma) and at 0, 15, 30, 60, 120, and 240 mins after treatment lysed with Western blots were performed using 4-20% Tris-glycine acrylamide gels (NuSep), Whatman Protran nitrocellulose membrane (Sigma) and developed with Pierce ECL substrate (ThermoFisher Scientific). Antibodies used were anti-HES5 [EPR15578] (Abcam, ab194111) and anti-alpha-tubulin (clone DM1A Sigma T9026). RNA half-life experiments were obtained by 10µM actinomycin D (ThermoFisher, Scientific) treatment of primary heterozygous Venus::HES5 and primary wild-type spinal cord NS cells. Samples were taken at 0, 15, 30, 45, 60, 80, 100, 120 mins after treatment and RNA prepared using RNAeasy kit (Qiagen) with DNAse treatment as per manufacturers instructions. cDNA was prepared using Superscript III (Invitrogen) as per manufacturers’ instructions and qPCR for Venus, HES5 and GAPDH was performed with Taqman (ThermoFisher, Scientific, UK) gene expression assays.

**Code and Data availability**

Data fitting for detections of oscillations has been implemented in Matlab R2015a using the GPML toolbox (Rasmussen and Hannes 2010) and custom designed routines available at [http://gaussianprocess.org/gpml/code/matlab/doc/](http://gaussianprocess.org/gpml/code/matlab/doc/). Code for stochastic model of genetic auto-repression and Bayesian inference available online under [https://github.com/kursawe/hesdynamics](https://github.com/kursawe/hesdynamics). Matlab custom designed routines for analysis of FCS available on request. Single-cell Venus::HES5, H2B::mCherry
intensity and positional information available on request from the corresponding authors.

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Author Contributions

CM and NP conceived and designed the experimental study. CM performed half-life experiments, acquired FCS data, acquired and analysed snapshot spinal cord slice images, acquired, tracked and analysed live spinal cord slice imaging movies, performed cluster analysis and cell positional/migration analysis, interpreted data and wrote the paper.

VB developed method to detect oscillations in noisy timeseries data and their period, amplitude and fold-changes, analysed expression dynamics in single-cell data and wrote code to identify cell neighbours and extract positional information from single-cell tracking.

JB wrote custom code to analyse FCS data by auto-correlation with model fit and number and brightness, optimized settings for FCS in tissue environment and aided acquisition and performed Q-Q analysis to generate quantitative expression map.

JK designed efficient implementation of stochastic and deterministic HES5 models, planned and performed Bayesian inference to parameterize both models, analysed both models and performed bifurcation analysis.

BY performed immunohistochemical staining for D/V progenitor domain markers to map Venus::HES5 expression domains.

DS assisted with optimization of settings for FCS in tissue environment and imaging of slice cultures.

CMS supervised and assisted analysis and interpretation of FCS data.

TG supervised and assisted analysis and interpretation of HES5 model.

MR supervised and assisted development of method to detect oscillations in noisy timeseries data.
NP supervised and directed the work and interpretation of data and co-wrote the paper with CM, VB and JK with input from JB and DS.

**Competing Financial interests**

None.
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Figure Legends

Figure 1. A quantitative map of HES5 expression across the dorso-ventral axis of the spinal cord

a) Transverse slice of live Venus::HES5 homozygous knock-in mouse spinal cord E10.5 ex vivo. Box identifies ventral domain, A-apical, B-basal. Scale bar 50µm. A-apical, B-basal. b) Immunofluorescence of E10.5 Venus::HES5 transverse slice of spinal cord ex-vivo. Sox2 – progenitors, NeuN - mature neurons and endogenous Venus::HES5 signal. Scale bar 30µm. c) Average FCS autocorrelation curve. 315 cells in homzygous Venus::HES5 spinal cord ventral region. Error bars - SD. Inset - example fluorescence count rate from single point within a nucleus in ex-vivo E10.5 Venus::HES5 slice. d) Nuclear Venus::HES5 concentration in ventral domain of homzygous E10.5 Venus::HES5 embryos measured by FCS. 315 cells, 4 experiments. Mean=140nM, SD=52nM. e) Transverse slice of live Venus::HES5 homozygous knock-in mouse spinal cord E10.5 ex vivo. Draq5 live nuclear stain. Scale bar 200µm. f) Regions of interest from nuclear segmentation of e) with grayscale Venus::HES5 intensity. g) Nuclear Venus::HES5 intensity (a.u) in a single live ex-vivo homozygous E10.5 Venus::HES5 transverse slice (e). 586 cells. Mean=61a.u SD=39a.u h) Nuclear Venus::HES5 concentration in homzygous E10.5 Venus::HES5 knock-in embryos across entire spinal cord measured by tissue FCS. 442 cells, 4 experiments. Mean is 148nM, SD=58nM. i) Quantile-quantile plot of nuclear Venus::HES5 concentration (h) vs nuclear Venus::HES5 intensity (g) for E10.5 homozygous embryos. Red line - linear fit over middle 90% range. j) Quantitative map of nuclear Venus::HES5 concentration in whole live E10.5 spinal cord. Intensity values scaled according to linear fit of Q-Q plot in i). Scale bar 50µm. k) Nuclear Venus::HES5 concentration by distance from ventricle in region 1 (upper box in j) and region 2 (lower box in j) l) Concentration difference between a cell and its nearest neighbours for cells less than or greater than 50µm (region 1) from the ventricle (n=154, n=73 respectively. p=0.0007 in Mann-Whitney test), or 30µm (region 2) from the ventricle (n=91, n=135 respectively. p<0.0001 in Mann-Whitney test). m) Coefficient of variation in Venus::HES5 intensity between cells less than or greater than 50µm from the ventricle in ventral domain in E10.5 Venus::HES5 embryos. (n=4 embryos, at least 24 cells per embryo, 2 experiments, p=0.04 in paired t-test.)

Figure 2. Hierarchical clustering reveals distinct Venus::HES5 expression dynamics

a) Schematic of snapshot Venus::HES5 intensity variability and possible non-mutually exclusive causes i) stable sub-populations of cells have different expression levels ii) single state of cell can traverse all intensity levels iii) cells undergo one-way transition from high to low levels of expression. b) Schematic of experimental approach to image Venus::HES5 expression dynamics from a single endogenous locus. c) Snapshot of ex-vivo live E10.5 Venus::HES5 Sox1Cre:ERT2 Rosa26RH2B::mCherry spinal cord slice culture. Scale bar 40µm. d) Example single cell traces of normalised Venus::HES5 protein expression in ex-vivo live E10.5
heterozygous Venus::HES5 spinal cord slice cultures. Individual H2B::mCherry+ cells were tracked over time in slice cultures. Single cell Venus::HES5 intensity values were normalised to the tissue mean intensity over time. e) Representative dendrogram from hierarchical clustering of standardised single cell Venus::HES5 protein dynamics in E10.5 heterozygous Venus::HES5 spinal cord slice culture in 1 experiment. Columns show standardised individual cell Venus::HES5 expression dynamics. Rows represent time points. 54 cells tracked for 12-hour time window with 15-minute frame intervals. f) Mean Venus::HES5 expression dynamics for cells in each cluster in a representative experiment corresponding to dendrogram in e). (Cluster 1 - 11 cells, cluster 2 - 11 cells, cluster 3 - 21 cells, cluster 4 - 11 cells). g) Example single cell traces for each cluster of normalised Venus::HES5 expression in ex-vivo live E10.5 spinal cord slice cultures. h) Left - coefficient of variation (C.O.V) of single-cell Venus::HES5 expression over time within 4, 8, 12,14 and 17.25 hour windows. Cluster 1 – black, cluster 2 – sky blue, cluster 3- green, cluster 4 – pink. 181 cells, 3 experiments, single points show C.O.V from a single-cell timeseries. Right - C.O.V in Venus::HES5 protein levels between cells measured at a single time point. 5 ex-vivo E10.5 Venus::HES5 slices in 2 experiments, single points show COV between cells in a single slice.

Figure 3. Distinct patterns of single-cell HES5 dynamics correspond to known cell-states and decision processes.

a) Example single-cell tracks for each cluster from 1 representative experiment. ‘*’ denotes cell division. Cluster 1 cell (black track) migrates to the apical surface and divides. Cluster 3 (green) and 4 (pink) cells move basally throughout 12-hour track. Dorso-ventral axis in µm from floorplate. b) Single cell tracks (n = 54) over 12-hours in a single E10.5 spinal cord slice movie. Black dotted line - ventricle. Grey - ventricular zone and green - mantle zone measured by Sox2/NeuN staining of 2 ex-vivo slices. c) Average distance of single cell from ventricle over 12-hour track. Cells clustered separately in 3 experiments. Kruskall-Wallis with Dunn’s multiple comparisons test indicated cluster 1 vs 3 adjusted p-value = 0.0014 d) Percentage of any cells found 0-25, 26-50, 51-75, 76-100 and 100-125µms from ventricle in each cluster. Stacked bars – mean, error bars - SD. 2-way ANOVA with Tukey multiple comparison test shows no difference between clusters <50µm from ventricle. 76-100µm from ventricle cluster 3 vs 1 p<0.0001, 3 vs 2 p=0.0009, 3 vs 4 p=0.014. e) Displacement of cells in each cluster. Dot - average start position, arrow - average finish position. f) Total distance travelled of single cells. Line is mean with SD. Kruskal-Wallis test with Dunn’s multiple comparison test shows cluster 1 vs 3 adjusted p=0.003, cluster 3 vs 4 adjusted p=0.0017. g) Percentage of cells per cluster undergoing 0 or 1 divisions in 12 hours. Chi-squared test of frequency data p=0.0002. 181 cells, 3 experiments clustered separately. Cluster 1 - black (n=27 cells), cluster 2 - sky blue (n=33 cells), cluster 3 - green (n=67 cells), cluster 4 - pink (n=54 cells) h) Relative Venus::HES5 intensity of E10.5 ex-vivo slices cultured in control DMSO (black) or 2µM DBZ (pink). Error bars - SD (3 experiments). Endpoint intensity - Mann Whitney two-tailed test p=0.0095. i) β-III tubulin (early neuronal marker) staining of DMSO or 2µM DBZ treated E10.5 ex-vivo slices. fp – floorplate. Scale bar 70µm. j) Displacement of single cells away from ventricle in apico-basal
axis in control DMSO or 2µM DBZ treated E10.5 slices. Bold line - average, dashed line - SD from 3 experiments. Two-tailed t-test p<0.0001. k) Hierarchical clustering of standardized single-cell Venus::HES5 expression in DMSO and 2µM DBZ treated E10.5 ex-vivo slices. 295 cells, 3 experiments clustered together. Cluster labels defined using clustering of DMSO alone. Pink – DMSO cells, green - DBZ cells. l) Percentage of cells in each cluster in DMSO and 2µM DBZ treated E10.5 ex-vivo slices. Frequency data subject to Chi-squared test showed p<0.0001. DMSO n=100 cells, 2µM DBZ n=195 cells, 3 experiments.

Figure 4. Cells undergoing state transition to neurons are more frequently oscillatory while proliferative progenitors are more noisy.

Example single-cell traces of Venus::HES5 expression subject to oscillatory test. a) Raw single-cell Venus::HES5 intensity timeseries with overlaid long-term trend in bold. b) Detrended single-cell Venus::HES5 intensity timeseries with overlaid OUOsc oscillatory model in bold. c) Percentage of single cells classified as having oscillatory Venus::HES5 protein expression in cluster 1+2 vs cluster 3+4. (n = 3 experiments, p-value = 0.04 in Wilcoxon paired test, two-tailed) Single-cell raw Venus intensity was detrended and subject to oscillatory test (Supp. methods). d) Single-cell periods of Venus::HES5 protein dynamics from oscillatory cells. Mean=3.3hours, SD=1.4hours. e). Noise in single cell Venus::HES5 expression dynamics per cluster as measured by the squared standard deviation of de-trended Venus::HES5 signal over time. Lines show mean with standard deviation. Kruskal-Wallis with Dunn’s multiple comparison test shows cluster 1 vs 3 adjusted p=0.04. 181 cells, 3 experiments clustered separately. Cluster 1 - black (n=27 cells), cluster 2 - sky blue (n=33 cells), cluster 3 - green (n=67 cells), cluster 4 - pink (n=54 cells). f) Likelihood of a cell having oscillatory Venus::HES5 expression indicated by LLR score plotted by average distance of the cell away from the ventricle over 12-hour track. Bars show mean and error bars show SEM. Kruskal-Wallis with Dunn’s multiple comparison test shows 0-25µm vs 26-50µm adjusted p=0.03. g) Noise in single cell Venus::HES5 expression dynamics plotted by average distance of the cell away from the ventricle over 12-hour track. Bars show mean and error bars show SEM. Kruskal-Wallis with Dunn’s multiple comparison test shows 0-25µm vs 26-50 adjusted p= 0.0007 and 0-25µm vs 50+µm adjusted p=<0.0001. h) Example single-cell timeseries of relative Venus::HES5 protein expression in ex-vivo live E10.5 Venus::HES5 spinal cord slice cultures showing noisy to oscillatory transition in Venus::HES5 dynamics.

Figure 5. The Hes5 oscillator is poised at the bifurcation point between aperiodic and oscillatory dynamics.

a) Schematic of stochastic model for genetic autorepression of HES5. b) Bayesian posterior model predictions of HES5 periods. Periods are extracted from simulated data of 12h duration using Hilbert transforms. Black line indicates mean of experimentally measured periods. Mean=4.47 hours, SD=2.51 hours. c) Distribution of model predicted relative standard deviations of HES5 expression over time. Mean =0.078, SD=0.023. The distribution approaches zero around 0.15, the experimentally
determined maximum value of standard deviation of Venus::HES5 over time (de-trended data) in proliferating progenitors in clusters 1 and 2 (Supp. Fig.9b). d) Ten example traces generated using the model are shown at three different parameter points in the panels i), ii), and iii). The power spectrum does not have a dominant non-zero peak in i) whereas the power spectra in ii) and iii) do have a dominant non-zero peak with decreasing width from ii) to iii) showing increasing coherence.

Parameter values are (i) $\alpha_m=0.64$/min, $\alpha_p=17.32$/min, $P_0=88,288.6$, $\tau=34$/min, $n=5.59$ (ii) $\alpha_m=39.93$/min, $\alpha_p=21.56$/min, $P_0=24,201.01$, $\tau=33$/min, $n=4.78$ (iii) $\alpha_m=44.9$/min, $\alpha_p=3.13$/min, $P_0=35,080.2$, $\tau=40$/min, $n=5.62$. The half-lives of the protein and mRNA are set to 90 and 30 minutes, respectively.

Figure 6. HES5 oscillations during transition to differentiation sculpt target gene expression.

a) Example single-cell timeseries of mean normalized Venus::HES5 expression (red) from cluster 3 showing amplitude death (amplitude indicated by dashed line). b) Instantaneous amplitudes from Hilbert transformation of de-trended single cell Venus::HES5 expression observed over time. Bars indicate mean and error bars indicate SD (121 cells from cluster 3 and 4 in 3 experiments clustered separately). Student’s t-test were used to compare maximum amplitude data in: cluster 3 (a) against subsequent timepoints showing significant decay after 10h (a,**: p= 0.0470), 12h -16h (a,***: p<0.0001); cluster 4 (b) against subsequent timepoints showing significant decay after 14h (b,**: p= 0.0153 and p=0.0195 for 14h and 16h respectively). c) Maximum peak-to-trough fold-change in single cell Venus::HES5 expression per cluster. Lines show mean and standard deviation. Kruskal-Wallis with Dunn’s multiple comparison test shows cluster 1 vs 3 adjusted p=0.0008, cluster 1 vs 4 adjusted p<0.0001. 181 cells, 3 experiments clustered separately. Cluster 1 (n=27 cells), cluster 2 (n=33 cells), cluster 3 (n=67 cells), cluster 4 (n=54 cells). d) Examples of single-cell Venus::HES5 timeseries in cluster 3 with oscillatory and non-oscillatory expression. Bold lines indicate model fit over normalized Venus::HES5 intensity. “+” indicates peak and “o” indicates trough in intensity values, fold-changes between peak-trough are indicated at relevant peak. e) Mean peak-to-trough fold-change in oscillatory (n= 52 cells, 3 experiments) or non-oscillatory (n = 69, 3 experiments) single-cell Venus::HES5 expression in differentiating cells in cluster 3 and 4. p=0.027 in Mann-Whitney test after 2 outliers removed. f) Model of Venus::HES5 expression dynamics through cell-state transition from neural progenitor cell to neuron. Neural progenitors have dynamic, noisy and aperiodic fluctuations in Venus::HES5 protein expression. As cells transition towards neurons
they have a long-term decreasing trend in Venus::HES5 and are more likely to show short-term oscillatory dynamics. As cells switch off Venus::HES5 oscillations decrease in amplitude.
Figure 1. A quantitative map of HES5 expression across the dorso-ventral axis of the spinal cord.

(a) Venus::HES5 Dorsal

(b) Venticle

Sox2 - progenitors

NeuN - neurons

Venus::HES5

(c) Venus::HES5 concentration (nM)

Relative frequency (%)

(lag time (s)

Nuclear Venus::HES5 fluorescence intensity (AU)

(d) Venus::HES5 concentration (nM)

Relative frequency (%)

(Venus::HES5 concentration (nM)

(e) Brightfield

Venus::HES5

Draq5

(f) Segmented Venus::HES5

(g) Manual segmentation

(h) FCS quantitation

(i) Nuclear Venus::HES5 fluorescence intensity (AU)

(j) Dorsal

HES5 concentration (nM)

(k) Region 1

Region 1

Region 2

(l) Region 1

Region 2

(m) Coefficient of variation (%) of Venus::HES5 between cells

(<50 µm) vs. (>50 µm)
Figure 2. Hierarchical clustering reveals distinct Venus::HES5 expression dynamics

**a**

Venus::HES5 heterogeneity

**b**

Dissect E10.5 embryos

**c**

Venus::HES5 expression

**d**

Venus::HES5 expression (Normalised to tissue mean) vs Time (hrs)

**e**

Cluster 1

**f**

Cluster 2

**g**

Cluster 3

**h**

Cluster 4
Figure 3. Distinct patterns of single-cell HES5 dynamics correlate with cell-states and decision processes.

(a) Diagram showing the relationship between distance from the ventricle and cluster index.
(b) Graph showing the average distance from the ventricle for different clusters.
(c) Bar graph showing the percentage of cells in different clusters.
(d) Graph showing the percentage of cells in different distance ranges.
(e) Scatter plot showing the relationship between cluster index and distance from the ventricle.
(f) Graph showing the total distance travelled in the apico-basal axis.
(g) Bar graph showing the percentage of cells with 0 or 1 division.
(h) Graph showing the relative Venus::HES5 intensity over time.
(i) Imaging of DAPI and β3-Tubulin under different treatments.
(j) Graph showing the distance from the ventricle under different treatments.
(k) Heatmap showing Venus::HES5 expression with different clusters and treatments.
(l) Bar graph showing the percentage of cells in different clusters and treatments.
Figure 4. Cells undergoing state transition to neurons are more frequently oscillatory while proliferative progenitors are more noisy.
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Figure 6. HES5 oscillations during transition to differentiation sculpt target gene expression

Legend:
- **Oscillatory**
  - Norm data
  - Model fit
  - Peaks
  - Troughs

- **Non-Oscillatory**
  - Norm data
  - Model fit
  - Peaks
  - Troughs

**Clustering:**
- Cluster 1 and 2
- Cluster 4 and 3

**Likelihood of being oscillatory:**
- Noisy progenitor
- Declining oscillatory differentiating cell

**Noise:**
- Noise
- Likelihood of being oscillatory