Evidence for X-ray emission in excess to the jet afterglow decay 3.5 yrs after the binary neutron star merger GW 170817: a new emission component

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ABSTRACT
For the first $\sim 3$ years after the binary neutron star merger event GW 170817 the radio and X-ray radiation has been dominated by emission from a structured jet initially propagating into a low-density medium with $n < 0.01 \text{cm}^{-3}$. We report on observational evidence for an excess of X-ray emission at $\delta t > 900$ days after the merger. With $L_x \approx 5 \times 10^{38} \text{erg s}^{-1}$ at 1234 days, the recently detected X-ray emission represents a $\geq 3.2 \sigma$ (Gaussian equivalent) deviation from the universal post jet-break model that best fits the multi-wavelength afterglow at earlier times. In the context of JetFit afterglow models, current data represent a departure with statistical significance $\geq 3.1 \sigma$, depending on the fireball collimation, with the most realistic models showing excesses at the level of $\geq 3.7 \sigma$. A lack of detectable 3 GHz radio emission suggests a harder broad-band spectrum than the jet afterglow. These properties are consistent with the emergence of a new emission component such as synchrotron radiation from a mildly relativistic shock generated by the expanding jet. In this context, we present a set of ab-initio numerical-relativity BNS merger simulations that show that an X-ray excess supports the presence of a high-velocity tail in the jet, and argues against the prompt collapse of the merger remnant into a black hole. Radiation from accretion processes on the compact-object remnant represents a viable alternative. Neither a kilonova afterglow nor accretion-powered emission have been observed before, as detections of BNS mergers at this phase of evolution are unprecedented.

1. INTRODUCTION

The binary neutron-star (BNS) merger GW 170817 is the first celestial object from which both gravitational waves (GWs) and light have been detected (Abbott et al. 2017a), enabling unprecedented insight on the pre-merger (GWs) and post-merger (light) physical properties of these phenomena (Margutti & Chornock 2021; Nakar 2020 and references therein). GWs from GW 170817 were detected on 17 August 2017 at 12:41:04 (UT) by Advanced LIGO and Advanced Virgo (Abbott et al. 2017b). The event was rapidly localized to reside in a nearby galaxy at a distance of 40.7 Mpc (Cantiello et al. 2018) thanks to the identification of its electromagnetic counterpart across the spectrum ($\gamma$-rays to radio, Abbott et al. 2017a). During the first $\sim 70$ days, the electromagnetic spectrum of GW 170817 consisted of a combination of thermal emission partially powered by the radioactive decay of heavy chemical elements freshly synthesized in the merger ejecta (i.e. the “kilonova”) and non-thermal synchrotron emission dominating in the X-ray and radio bands. The spectrum and flux evolution of the kilonova emission from GW 170817 was in agreement with theoretical predictions (Metzger 2017) demonstrating that mergers of neutron stars are one of the major sources of heavy elements in our Universe (e.g., Rosswog et al. 2018). Modeling of the UV-Optical-NIR thermal emission from the kilonova allowed estimates of the bulk velocities and masses of the slower-moving ejecta powering the kilonova: $v \sim 0.1 - 0.3c$ and total ejecta mass $M_{ej} \sim 0.06 M_\odot$, carrying a kinetic energy of $\approx 10^{51} \text{erg}$ (Villar et al. 2017; Cowperthwaite et al. 2017; Drout et al. 2017; Kilpatrick et al. 2017; Arcavi 2018; Waxman et al. 2018; Bulla et al. 2019; Nicholl et al. 2021).

In the first $\approx 900$ days since merger, the non-thermal spectrum of GW 170817 has been dominated by synchrotron emission from an ultra-relativistic structured jet initially pointing $\theta_{\text{obs}} \sim 15 - 25$ degrees away from our line of sight (Mooley et al. 2018a; Ghirlanda et al. 2019; Hotokezaka et al. 2019; Nathaniel et al. 2021). Radio-to-X-ray data did not show any evidence for spectral evolution across nine orders of magnitude of frequency for 900 days (Fong et al. 2019; Hajela et al. 2019; Troja et al. 2020) and the emission was well characterized as originating from an optically thin synchrotron source with a power-law spectrum $F_\nu \propto \nu^{-(p-1)/2}$ with best-fitting $p = 2.160 \pm 0.026$ (Fong et al. 2019), where $p$ is the index of the distribution of relativistic electrons responsible for the emission $dN_e/d\gamma_e \propto \gamma_e^{-p}$, and $\gamma_e$ is the electron Lorentz factor above some minimum Lorentz factor $\gamma_{\text{min}}$. Modeling of the multi-wavelength off-axis jet afterglow emission enabled tight constraints on some of the system and environment parameters (or their combination): for example, the jet kinetic energy to environment density ratio was constrained to $E_k/n \approx (1 - 2) \times 10^{53} \text{erg cm}^{-3}$ (Mooley et al. 2018a; Ghirlanda et al. 2019; Hotokezaka et al. 2019) with a credible density range of $10^{-4} \text{cm}^{-3} \leq n \leq 10^{-2} \text{cm}^{-3}$ (Hajela et al. 2019) and the inferred ultra-relativistic jet opening angle is $\theta_{\text{jet}} \approx 2 - 5$ degrees (Mooley et al. 2018a; Ghirlanda et al. 2019; Hotokezaka et al. 2019; Nathaniel et al. 2021). A robust prediction of the off-axis afterglow model post-peak (i.e. after radiation from the core of the jet enters the observer’s line of sight) is that of a universal asymptotic light-curve decay with flux $F_\nu(t) \propto t^{-p}$ (Sari et al. 1999). For the best-fitting jet-environment parameters of GW 170817 no broadband spectral evolution is expected, leading to $F_\nu(t) \propto t_{-p}$ (we call this the “universal post jet-break model”). Until $\approx 900$ days post-merger, panchromatic observations of the jet afterglow of GW 170817 satisfied these expectations.

Here we present the results from our multi-wavelength campaign of GW 170817 at X-ray and radio frequencies extending to 1273 days since merger, which was designed to constrain the emergence of the kilonova afterglow. These observations provide the first statistically significant evidence for an excess of X-ray emission that is consistent with the emergence of a new X-ray component of emission that is physically distinct from the jet afterglow. This paper is organized as follows. In §2, we present the detailed analysis of the recent X-ray observations taken at $\delta t = 1234$ days and a re-analysis of the observations at $\delta t \sim 939$ days and

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earlier. Newly acquired VLA and MeerKAT observations around $\delta t = 1234$ days are presented in §3. We calculate the statistical evidence for the observed excess of emission in X-rays in §4. We discuss the inferences of the observed excess in X-rays and a lack of detection in radio on the broadband spectrum in §5. We discuss the possibility of different scenarios leading to an excess in X-rays without an accompanying radio emission as the observations suggest in §6–§8. We draw our conclusions in §9.

2. X-RAY OBSERVATIONS

We present Chandra X-ray Observatory (CXO) observations of the X-ray emission from GW 170817 acquired at $\delta t = 1209 – 1258$ days since merger (combined X-ray image in the left panel in Figure 1) and a complete and homogeneous analysis of the entire CXO data set. Results from CXO observations of the jet afterglow of GW 170817 in the time range $\delta t = 2.33 – 939.31$ days have already been published in the literature (Margutti et al. 2017; Haggard et al. 2017; Margutti et al. 2018; Nynka et al. 2018; Alexander et al. 2018; Troja et al. 2018; Ruan et al. 2018; Pooley et al. 2018; Piro et al. 2019; Troja et al. 2019; Hajela et al. 2019, 2020; Troja et al. 2020; Makhathini et al. 2020). With respect to previous data reductions: (1) when possible, we do not assume a spectral model for the X-ray count-to-flux calibration, which allows us to test for spectral evolution; (2) we align all the X-ray images to a common astrometric solution, significantly improving on the CXO relative astrometry; (3) for each observation we extract a spectrum and we perform a flux calibration that utilizes the complete information on the instrumental response at the time of the observation (as opposed to using averaged instrumental responses); (4) we jointly fit spectra from observations acquired close in time (i.e., around the same “epoch”) as opposed to merging the files into an average spectrum; (5) we implement an accurate point-spread function (PSF) correction; (6) we calculate the model parameter uncertainties (including the unabsorbed fluxes) with MCMC simulations that self-consistently account for the low-count statistics and the deviation from Gaussian statistics. At $\delta t > 900$ days, the low number statistics of the detected X-rays does not allow us to independently constrain the spectral model and we thus offer a flux calibration that assumes the jet-afterglow spectral parameters.

2.1. CXO Source Count Rates

We observed GW 170817 with the CXO from December 09, 2020 at 00:05:21 UT through December 13, 2020 at 14:02:43 UT, and further between January 18, 2021 at 09:43:15 UT and January 27, 2021 at 08:49:13 UT, spanning $\delta t = 1209 – 1258$ days after the merger. The observation was taken in seven distinct exposures (Obs ID 22677, 24887, 24888, 24889, 23870, 24923, and 24924; PI Margutti; programs #21510449 and #22510329, publicly available on the CXO archive) for a total exposure time of 189.1 ks.

We reprocessed the entire CXO dataset using the reproc task within CIAO (v4.13.0, Fruscione et al. 2006) with standard ACIS data filtering and using the latest calibration database (CALDB, v4.9.4). We used wcs_match and wcs_update to realign all the IDs to a common astrometric solution using as a reference the list of X-ray point-source positions generated with wavdetect run on our longest exposure observation (Obs ID 20860). In ID 20860 the X-ray emission from GW 170817 is detected with high significance at sky coordinates RA=13.0°09.48′.061 ± 0.049″ and dec=−23°.22′:52.88″ ± 0.034″ (J2000). After having realigned the images, for each ID we extracted source count-rates and spectra using a 1″ region centered at the coordinates above. Table 1 lists the inferred 0.5 – 8 keV net count-rates and the associated target-detection significance. For source detection, we employed a 1″ source region and we filtered in the energy range 0.5 – 8 keV to minimize the background contribution. For reference, a 1″ region contains $\geq 90%$ of the PSF at 1 keV.

Focusing on the data at $\delta t > 900$ days, we find that an X-ray source is clearly detected at the location of GW 170817 at $\delta t = 939$ days with a statistical significance of 5.4 $\sigma$ (Gaussian equivalent), corresponding to a net count-rate of $(7.53 \pm 2.93) \times 10^{-5}$ ct s$^{-1}$ (0.5 – 8 keV). For CXO observations acquired at $\delta t = 1209 – 1214$ days, we infer an observed net count-rate of $(1.13 \pm 0.36) \times 10^{-5}$ ct s$^{-1}$ (6.3 $\sigma$ detection significance), whereas for the remaining observations acquired between $\delta t = 1250 – 1258$ days, the observed net count-rate is $(4.31 \pm 2.28) \times 10^{-5}$ ct s$^{-1}$ and an X-ray source is detected at a significance level of 3.4 $\sigma$. Being temporally close, we combined the latter two sets of observations spanning 1205 – 1258 days and we infer a net count-rate of $(7.68 \pm 2.12) \times 10^{-5}$ ct s$^{-1}$, where an X-ray source is detected with a 7.2 $\sigma$ statistical significance.

2.2. CXO Spectral Analysis

For each re-aligned Obs ID we extracted a spectrum using a 1″ circular source region centered at the location of the X-ray counterpart of GW 170817 indicated above and a source-free background region of 22″. We used specextar, setting the refcoord parameter to the center of the source region to ensure an accurate PSF correction to the inferred fluxes. This procedure furthermore ensures that the appropriate instrumental ARF (Auxiliary Response File) and RMF (Redistribution Matrix File) response files are generated for each Obs ID. We note that not setting refcoord parameter explicitly leads to an overestimate of the PSF correction by an average factor of $\approx 1.2 – 1.5$ for a source region of 1″. We fitted the data with an absorbed power-law spectral model (tbabs*ztbabs*cflux(pow)) within Xspec (v12.9.1). We adopted a Galactic neutral hydrogen column density in the direction of GW 170817 of $N_{\text{H}} = 7.84 \times 10^{21}$ cm$^{-2}$ (Kalberla et al. 2005). Consistent with results from previous analysis (Margutti et al. 2017, 2018; Alexander et al. 2018; Hajela et al. 2019; Makhathini et al. 2020), we did not find evidence for intrinsic absorption and we thus assumed no intrinsic absorption in the following analysis. For $\delta t < 750$ days, we jointly fitted the observations acquired around the same epoch since merger leaving the spectral photon index, $\Gamma$, and the unabsorbed 0.3 – 10 keV flux as free pa-
parameters. We fitted the data in the 0.3–10 keV energy range. We note that filtering the data in the 0.5–8 keV energy range before fitting does not lead to significantly different inferences. We used Cash statistics and we employed a chain of $10^5$ MCMC simulations to estimate the parameter uncertainties to account for the deviation from Gaussian statistics in the regime of low counts. The results from our X-ray spectral modeling are reported in Table 1. We find no evidence for X-ray spectral evolution of the source at $\delta t < 745$ days. From a joint spectral fit of all CXO observations at $\delta t < 745$ days with the same $\Gamma$ we infer a best-fitting $\Gamma = 1.603^{+0.102}_{-0.070}$ consistent with our previous analysis of these observations in Hajela et al. 2019 which used a previous CALDB v4.8.3 and a 1.5" source region.

We now consider the CXO observations acquired at $\delta t > 745$ days. These CXO observations were acquired in two epochs at $\delta t = 939$ and $\delta t = 1234$ days since merger. The low-count statistics of 6 and 12 photons, respectively, available for model fitting after Xspec filtering in the 0.3–10 keV energy range leads to poorly constrained spectral photon indexes $\Gamma = 1.16^{+1.35}_{-0.94}$ and $\Gamma = 1.92^{+0.53}_{-0.65}$. We thus proceeded by freezing the spectral photon index to $\Gamma = 1.603$ (i.e. the best-fit value inferred from the joint fit of all the CXO data collected at $\delta t < 745$ days) for the purpose of count-to-flux calibration. The inferred unabsorbed 0.3–10 keV flux is $F_x = 1.81^{+0.79}_{-0.94} \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ at $\delta t = 939$ days, and $F_x = 2.31^{+0.57}_{-0.81} \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ at $\delta t = 1234$ days, corresponding to luminosities of $L_x \approx (3-5) \times 10^{38}$ erg s$^{-1}$ (Table 1). These recent observations when visually examined against the jet afterglow model that best-fitted the multiwavelength data at $\delta t < 745$ days (Figure 2) show slight deviations from the expectations. We quantify this deviation in Section 4.

We end by addressing the possibility of X-ray spectral evolution at $\delta t > 745$ days. We assessed the statistical evidence for X-ray spectral evolution in two ways. First, from a joint spectral modeling of all CXO data acquired at $\delta t > 745$ days with a power-law spectrum, we infer $\Gamma = 1.54^{+0.83}_{-0.75}$. Compared to $\Gamma = 1.603^{+0.102}_{-0.070}$ of the earlier X-ray data reported above, we find that there is no evidence for statistically significant X-ray spectral evolution from this analysis. Second, we generated $10^6$ synthetic spectra of $N = 12$ photons (as observed at $\delta t = 1234$ days in the 0.3–10 keV energy range after Xspec filtering) by randomly sampling the probability density distribution associated with an incoming $\Gamma = 1.6$ spectrum with $N_{\text{gal}} = 7.84 \times 10^{20}$ cm$^{-2}$ convolved with the CXO instrumental response. We applied the non-parametric distribution-free Epps–Singleton two-sample test to each sample and the parent distribution and we found that 52% of the synthetic samples have a p-value at least as extreme as the one associated with the observed photon distribution, leading to no statistical evidence of a departure of the detected photon distribution at $\delta t > 745$ days from earlier X-ray data. We conclude that there is no statistically significant evidence for the evolution of the X-ray spectrum at $\delta t > 745$ days.

Finally, we compare the results from our X-ray analysis with previous results that appeared in the literature, and specifically with the analyses by Troja et al. 2020 (for $\delta t = 582 - 945$ days), Makhathini et al. 2020 (for $\delta t = 9 - 745$ days) and Troja et al. (2021). The analysis by Makhathini et al. (2020) cannot be used to test for X-ray spectral evolution of the source because the final count-to-flux calibration is performed by assuming a spectral photon index. We find that the central values of the X-ray fluxes reported by Makhathini et al. (2020) using a 1" source region are systematically larger than our fluxes (by a factor of up to 30%). Discrepancy remains even after adopting the same $\Gamma = 1.57$ for the count-to-flux calibration. We are able to reproduce the Makhathini et al. (2020) X-ray fluxes by removing the reftcords parameter setting from specext, which leads to artificially inflated PSF corrections of $\approx 20 - 50\%$, as previously noted. Our X-ray fluxes in the time range $\delta t = 582 - 945$ days are consistent with those reported by Troja et al. (2020) within 1-$\sigma$ uncertainties. We found that we
Figure 2. X-ray (upper panel) and radio (3 GHz, lower panel) evolution of the emission from GW 170817 as detected by the CXO and the VLA (light-blue circles). Open circle: peak pixel flux value within one synthesized beam at the location of GW 170817 from Balasubramanian et al. 2021. At δt > 900 days the X-ray emission shows an excess compared to the off-axis jet afterglow model (solid blue line, §4 and §6) that indicates the emergence of a new emission component. Red-to-orange dashed lines: synchrotron radiation from the kilonova afterglow calculated using semi-analytical models (Kathirgamaraju et al. 2019) where we parametrized the kilonova kinetic energy distribution as \( E_k \propto (\Gamma \beta)^{-\alpha} \) for \( \beta \geq 0.35 \) and we used a total kilonova kinetic energy of \( 10^{51} \) erg. These models require \( p < 2.15 \) to avoid violating our radio upper limit. Here we use \( p = 2.05 \) and we emphasize with a solid thick line the \( \alpha = 5 \) model. Other kilonova afterglow parameters assumed: \( \epsilon_B = 0.001, \epsilon_e = 0.1, n = 0.001 \) cm\(^{-3} \). Grey shaded area: synchrotron emission calculated from kilonova kinetic ejecta profiles derived from ab-initio numerical relativity simulations using a neutron-star mass-ratio \( q = 1 \) and the LS220 equation of state (§7). These simulations emphasize the contribution from the merger’s dynamical ejecta. The shaded area corresponds to values \( p_{KN} = 2.05 - 2.15, n = 6 \times 10^{-3} \) cm\(^{-3} \), \( \epsilon_e = 0.1 \) and \( \epsilon_B = 0.01 \).
could reproduce the Troja et al. (2020) fluxes by using the online Portable Interactive Multi-Mission Simulator (PIMMS) for the count-rate to flux calibration. In contrast, our spectral analysis and count-to-flux calibration is based on ARFs and RMFs generated from each individual Obs ID to best account for the instrumental response at the time and in the conditions of the observation, as opposed to the proposal planning tool PIMMS.

We finally compare our results with the recent work of Troja et al. (2021), which appeared after our first submission to the archive, where their fiducial X-ray fluxes are calculated by adopting a photon index $\Gamma = 1.585$ derived from their modeling of the broadband radio-to-X-ray afterglow spectrum, differently from our jet afterglow model-independent analysis. The count-to-flux calibration by Troja et al. (2021) is done by using the hardness ratio (HR) of observed counts in the $0.5 - 2$ keV energy range and the $2 - 7$ keV energy range to infer a spectral photon index, as opposed to the full spectral extraction and analysis that we perform here. The HR method does not account for and does not self-consistently model the uncertainty that affects the energy of each event on the detector. It is furthermore based on averaged instrumental responses (one for each epoch), instead of using the accurate instrumental information from each Obs ID, which our joint spectral analysis does. While we emphasize that there is no tension between the derived $0.3 - 10$ keV fluxes of the two methods and the fluxes are consistent to within $1\sigma$ uncertainties\(^1\) (Figure 12), here we note the following: (i) as there is no evidence of the latest radio and X-ray observations at $\delta t = 1234$ days lying on the same power-law segment of the spectrum, no such assumption is made for the flux calibration of the X-ray data. (ii) We self-consistently propagate the uncertainties during the spectral calibration. (iii) The X-ray upper limit at 2 days is computed using pure Poisson statistics and represents the $3\sigma$ deviation from the background, as we detail in Margutti et al. (2017). The difference in the flux limit is partially a result of the different photon indexes assumed by Troja et al. (2021) ($\Gamma = 1.585$) and Margutti et al. (2017) ($\Gamma = 2$) for the spectral calibration of the count-rate upper limit. Unsurprisingly, models with harder assumed photon indices lead to greater $0.3 - 10$ keV fluxes.

3. RADIO OBSERVATIONS

3.1. VLA Data Analysis

\(^1\)https://cxc.harvard.edu/ciao/why/pimms.html

\(^2\)For observations taken at $\delta t = 1234$ day, assuming $NH_{gal} = 1.1 \times 10^{22}$ cm$^{-2}$ and $\Gamma = 1.585$, as in Troja et al. (2021), we find an unabsorbed $0.3-10$ keV flux of $1.8_{-0.4}^{+0.2} \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ when using an averaged instrumental response, which is entirely consistent with $F_x = 1.6_{-0.5}^{+0.6} \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$ reported by Troja et al. (2021) for the same model parameters. Instead, using the more accurate approach of jointly fitting the observations, each with its own instrumental response, and using the same parameters $NH_{gal} = 1.1 \times 10^{22}$ cm$^{-2}$ and $\Gamma = 1.585$, we find an unabsorbed flux of $2.51_{-0.92}^{+0.69} \times 10^{-15}$ erg cm$^{-2}$ s$^{-1}$, which is consistent to our value. All errors are quoted at 68% confidence level.

We initiated late-time S and Ku-band Karl G. Jansky Very Large Array (VLA) observations of GW 170817 as part of our joint CXO-VLA proposals #21510449 and #22510329 (PI Margutti). GW 170817 was observed for a total of 10.21 hours on source at S-band spread between three observations occurring on 15\(^{th}\) December 2020 ($\delta t = 1216.08$), 27\(^{th}\) December 2020 ($\delta t = 1228.02$) and 2\(^{nd}\) February 2021 ($\delta t = 1264.95$). All three observations were conducted while the VLA was in A-configuration and at a central frequency of 3 GHz using a 2 GHz bandwidth. Additionally, we conducted a single observation at Ku-band on 10\(^{th}\) February 2021 ($\delta t=1272.88$) for a total of 2.74 hours on source. The observation was conducted with the VLA in A-configuration and at a central frequency of 15 GHz using a 6 GHz bandwidth. These data are publicly available on the VLA archive under project IDs SL0449 and SM0329. Details of each observation are given in Table 2.

Each individual observation was independently calibrated using the VLA calibration pipeline version 2020.1.0.36 as part of CASA (v6.1.2.7, McMullin et al. 2007), with 3C286 used as the flux density and bandpass calibrator and J1258-2219 used to calibrate the time-varying complex gains. We then manually inspected and validated the output and re-ran the pipeline after flagging additional radio frequency interference (RFI). Additional RFI flagging was performed on the results of the second pipeline run. In order to achieve maximum sensitivity we combined the three epochs of S-band data into a single measurement set (right panel in Figure 1) using the CASA task concat. We imaged the concatenated data using wsclean (Offringa et al. 2014; Offringa & Smirnov 2017), creating a 16384 × 16384 pixel image with a single pixel corresponding to 0.08″. The synthesised beam is 1.19″ × 0.60″ with a position angle of −5.57 degrees. In order to account for spectral variation introduced for sources far from the phase center, we are imaging well beyond the half power point of the primary beam in order to ensure complete deconvolution, and to produce an accurate sky model for self-calibration we fit a third order polynomial (fit-spectral-pol 4) over eight output channels (channels-out 64). No time or frequency averaging was performed when imaging in order to avoid bandwidth or temporal smearing of sources far from the phase center ensuring the best possible deconvolution. We performed one round of phase-only self-calibration using a sky-model produced from our phase reference calibrated data.

We do not detect any significant emission at the position of GW 170817. The root-mean-square (RMS) noise at the edge of the image in a region free of sources is $\sim 1.2 \mu$Jy while in a circular region with 25 pixel radius centered on the position of GW 170817 we measure an RMS noise of $\sim 1.7 \mu$Jy.

The single Ku-band epoch was calibrated using the VLA calibration pipeline version 2020.1.0.36 as part of CASA version 6.1.2.7 and validated by NRAO as part of the Science Ready Data Products project. We imaged the calibrated measurement set using the CASA task tclean with a user defined mask. We created a 2048 × 2048 pixel image with a cell size of 0.02″. We do not detect any significant emission at
the location of GW 170817 and measure an RMS noise of 1.7 \(\mu\)Jy in a 30 \(\times\) 30 pixel region centred on the position of GW 170817.

3.2. \textit{MeerKAT Data Analysis}

We conducted a single observation of the field of GW 170817 with the MeerKAT radio interferometer on the 3\textsuperscript{rd} January 2021 as part of a DDT request (DDT-20201218-JB-01). These data are available publicly on the SARAO archive. Data were recorded for a total of 7.56 hours (resulting in 7.24 hours on source) with an 8 s dump time at the UHF band between 544 MHz and 1088 MHz with a central frequency of 816 MHz using 4096 frequency channels. Details of the observation are given in Table 2.

Data reduction was performed using \textsc{oxkat} (Heywood 2020), a suite of semi-automated scripts to reduce MeerKAT UHF and L-band data. First, phase reference calibration (1GC) is carried out using CASA, with flagging performed with Tricolour (a variant of the SARAO Science Data Processing flagging software). B0407−65 was observed to calibrate the flux and bandpass of the instrument and 3C283 was used to calibrate the time variable complex gains. Second, we used \textsc{wsclean} to image the field and the resulting sky model was used to perform phase and delay self-calibration (2GC) using \textsc{cubical} (Kenyon et al. 2018). Images created throughout this process are 10240 \(\times\) 10240 pixels with a robust weighting of −0.5 and pixel size of 1.7”. The phase calibrator, 3C283, is a bright off-axis source when observing GW 170817 with MeerKAT at the UHF band and leaves strong imaging artefacts after 2GC calibration. Strong sources away from the phase center of an interferometer have their apparent spectral shape modified by the time and frequency dependent primary beam, and for a sufficiently wide field of view one set of gain solutions (direction-dependent) is not appropriate to properly calibrate the data. These issues result in a corrupted point spread function that will not vanish under deconvolution. The primary beam can be corrected for either by providing a model of the primary beam for the array, or by using higher order polynomials when fitting the spectral variation when cleaning (\textsc{oxkat} employs the latter). To correct for direction-dependent gains across the wide MeerKAT field of view (∼ 2 \(\deg\)\(^2\) at UHF) we ‘peel’ the source 3C283, and performed faceted direction dependent self-calibration on the residual data. The peeling stage was performed using \textsc{cubical}, and the facet based direction dependent calibration was carried out using \textsc{killms} with \textsc{ddfacet} (Tasse et al. 2018) used to image the corrected data. To enhance the resolution we image the final data-set with a Briggs robustness parameter −1.

The RMS noise at the edge of the image in a region free of sources is 8.5 \(\mu\)Jy. Due to the extremely high source brightness sensitivity of MeerKAT the region around the phase center has a very high density of sources, making it difficult to estimate the phase center noise. We opt to fit the entire image for significant emission using \textsc{PyBDSF} (Mohan & Rafferty 2015) using island and pixel thresholds of 3\(\sigma\) and 5\(\sigma\), respectively, with adaptive RMS thresholding turned on. We identify extended (resolved) emission from the host galaxy of GW 170817 (NGC 4993) and emission from a source. We identify no significant emission at the position of GW 170817. Using a 40 \(\times\) 40 pixel region centered on the position of GW 170817 we measure an RMS noise of \(\sim 13 \mu\)Jy.

4. \textbf{STATISTICAL EVIDENCE FOR AN X-RAY EXCESS OF EMISSION}

In this section, we calculate the significance of a deviation, if any, of the latest X-ray observations from jet afterglow models. We perform our statistical analysis in the count phase-space to fully account for the Poissonian nature of the process. Our results and conclusions do not depend on the specific flux calibration of the latest epochs of data at \(\delta t > 900\) days that we present in Table 1 with the purpose of offering to the reader a flux scale, and we explain the reasons as follows. Our goal is to test for the presence of a departure from the expectations of jet afterglow models, which have solid predictions both in terms of temporal behavior and in terms of spectral behavior of the data at \(\delta t > 900\) days. Jet models can be violated spectrally, temporally, or both spectrally and temporally. The X-ray data at \(\delta t > 900\) days provide no useful spectral constraint (§2.2). At this point we face two options: (i) we can perform a flux calibration of the X-ray count-rates at \(\delta t > 900\) days assuming a spectral model that is \textit{not} consistent with jet afterglows. This clearly violates jet afterglow models and implies that these models can be rejected at late times, and that the late-time X-rays come from a different source of emission; or (ii) we conservatively assume that the late-time X-rays have a spectrum that is consistent with jet afterglow models and we use the range of spectral models that are statistically allowed by jet afterglows to convert the predicted fluxes into observed count-rates on the CXO detector. We adopt approach (ii). This approach is conservative, in the sense that we are \textit{assuming} that the late-time X-ray spectrum is exactly as expected based on jet afterglow models, while in fact this might not be true. With this assumption, we then address the question: what is the probability of detecting a number of X-ray photons at least as large as the one observed at \(\delta t > 900\) days as a result of a statistical fluctuation of the model and background? In the following we first adopt a jet-structure model agnostic approach, and use the universal post jet-break model to assess the potential deviation of the late-time X-ray data (§4.1). Second, we use the off-axis structured jet afterglow models as computed by \textsc{JetFit} (§4.2). Finally, we address in detail potential sources of systematic uncertainties and the performance of other numerical afterglow models. For the remainder of this section we note that including or not including in the initial jet afterglow fitting procedure the X-ray data at \(\delta t > 900\) days leads to differences that are smaller than the quoted level of precision of the statistical significances of the departure of the data from the models. This is a direct consequence of the limited number of X-ray photons at \(\delta t > 900\) days, which leaves the X-ray flux fundamentally unconstrained (§2.2). We elected to fit the data at \(\delta t < 900\)
days, which has the advantage of preserving the statistical independence of the data acquired at $\delta t > 900$ days from the models we are testing. We end by noting that from a statistical perspective we are not comparing two sets of models. Instead, we are assessing the potential departure of a subsample of data from models of jet afterglow emission.

4.1. Jet afterglows from the universal post jet-break model

We first assessed the statistical evidence of an excess of X-ray emission with respect to the off-axis jet afterglow model by fitting the post-peak multi-wavelength afterglow decay with the following model $F_\nu \propto \nu^{-\beta}t^{-\alpha}$. The X-ray to radio emission of GW 170817 is powered by synchrotron radiation in the optically thin regime (Margutti et al. 2018; Fong et al. 2019) for which $\beta = (p-1)/2$. Standard closure relations (e.g., Lamb et al. 2018) in the post jet break phase, which apply to the post-peak afterglow evolution, imply $\alpha = p$ (Sari et al. 1999). Our “universal post jet-break model” is thus: $F_\nu \propto \nu^{-(p-1)/2}t^{-p}$. The multi-wavelength jet afterglow of GW 170817 peaked at $t_{\text{pk}} \approx 160$ days (Dobie et al. 2018; Alexander et al. 2017; Mooley et al. 2018b).

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**Figure 3.** Top Panel: Universal post jet-break model distributions. Expected 1-keV flux density distributions at 939.31 and 1234.11 days (histograms in color) derived from fitting the post-peak multi-wavelength afterglow of GW170817 in the post jet-break regime with $F_\nu \propto \nu^{-\beta}t^{-\alpha}$ (where $\beta = (p-1)/2$ and $\alpha = p$) in the time range $t_{\text{start}} < \delta t < 900$ days for a variety of choices of $t_{\text{start}}$. Bottom Panel: JetFit model distributions. Expected 1-keV flux density distributions at 939.31 and 1234.11 days (histograms in color) derived from the fitting of the multi-wavelength afterglow of GW170817 in the time range $2 < \delta t < 900$ days using the code JetFit (using different values of $\gamma_0$). Both Panels: Vertical blue thick line and shaded area: observed X-ray flux density at the corresponding epoch and $\pm 1\sigma$ confidence range, for which the flux calibration was performed by conservatively assuming a jet-afterglow spectrum ($\S$2.2- $\S$4).
We fitted the multi-wavelength post-peak jet afterglow evolution with the model above in the time range $t_{\text{start}} < \delta t < 900$ days for several choices of start time $t_{\text{start}} = 157, 163, 172, 196, 209, 215, 230$ days. We selected a range of $t_{\text{start}}$ times starting from $t_{\text{ph}}$ to account for the unknown onset time of the asymptotic post-peak jet-break power-law decay. We used VLA observations at 3 and 6 GHz compiled from Hallinan et al. 2017; Alexander et al. 2017; Mooley et al. 2018c; Margutti et al. 2018; Dobie et al. 2018; Alexander et al. 2018a; Hajela et al. 2018b; Margutti et al. 2018; Dobie et al. 2018; Alexander et al. 2018; Mooley et al. 2018a; Hajela et al. 2019; Hubble Space Telescope (HST) observations at optical wavelengths from Fong et al. 2019; and CXO observations at 1 keV from this work. As an example, we show the plot of the best-fitting model, and the corresponding 68% confidence interval, obtained assuming $t_{\text{start}} = 196$ days in Figure 4. We assess the statistical significance of the departure of the late-time X-ray data for each choice of $t_{\text{start}}$.

We employed MCMC sampling with a Python module, `emcee` (Foreman-Mackey et al. 2013). For each choice of $t_{\text{start}}$ we sampled $10^5$ times the expected X-ray flux density distribution at 1 keV ($F_{1}\text{keV}$) at the times of the last two CXO epochs at $t_1 = 939.31$ days and $t_2 = 1234.11$ days (Table 1, top panel in Figure 3). For each MCMC sample we converted the predicted 1-keV flux densities ($F_{1}\text{keV},1 \equiv F_{1}\text{keV}(t_1)$ and $F_{1}\text{keV},2 \equiv F_{1}\text{keV}(t_2)$) into observed 0.5–8 keV total (i.e. source plus background) counts in a $1''$ region ($c_1$ and $c_2$) using the respective exposure times, the count-to-flux conversion factors derived from Xspec and the observed background. We computed for each MCMC sample $i$ the probabilities $P_{1,1} \equiv \text{Pois}(c \geq N_{\text{obs},1}(c_1)$ and $P_{1,2} \equiv \text{Pois}(c \geq N_{\text{obs},2}(c_2)$, which represent the probability of each sample to produce a number of X-ray photons larger or equal to those observed at $t_1$ and $t_2$ after Xspec filtering in the 0.5–8 keV energy band ($N_{\text{obs},1} = 6$ and $N_{\text{obs},2} = 12$, as noted in §2.2) as a result of a Poissonian fluctuation. For each model defined by the choice of $t_{\text{start}}$, the total probability to lead to a deviation at least as prominent as the one observed at $t_1$ and $t_2$ is the re-normalized sum of the sample probabilities: $P_{1} = \frac{1}{N_{\text{sample}}} \sum_i P_{1,i}$ and $P_{2} = \frac{1}{N_{\text{sample}}} \sum_i P_{2,i}$. We find that the resulting $P_1$ and $P_2$ vary in the range $P_1 = 0.060 - 0.139$ and $P_2 = 2.61 \times 10^{-4} - 1.53 \times 10^{-3}$ depending on the choice of $t_{\text{start}}$. The observed X-rays at 1234 days thus correspond to a 3.2$\sigma$ - 3.7$\sigma$ (Gaussian equivalent, 99.8626% - 99.9784%) deviation from the off-axis jet model. $P_{1} \times P_{2}$ thus lies in the range $P_{1} \times P_{2} = 1.73 \times 10^{-9} - 2.50 \times 10^{-4}$, where the range of probabilities reported reflect the assumed $t_{\text{start}}$ (Table 3). Finally, the combined probability to obtain deviations from the universal post-jet break off-axis model at 939.31 days and 1234.11 days can be conservatively estimated as $P_{\text{combined}} = \frac{1}{N_{\text{sample}}} \sum_i \text{Pois}(c \geq (N_{\text{obs},2} + N_{\text{obs},1})(c_1 + c_2,1))$. We find $P_{\text{combined}} = 9.51 \times 10^{-5} - 1.37 \times 10^{-3}$ (3.2-3.9$\sigma$, Gaussian equivalent, depending on the choice of $t_{\text{start}}$). We conclude that the observed X-rays at $\delta t > 900$ days represent a statistical deviation from the expectations of the universal post jet-break models that best fit earlier observations of GW 170817 with statistical significance $\geq 3.2\sigma$. The chance probabilities as a function of $t_{\text{start}}$ are reported in Table 3.

4.2. Jet afterglows computed with JetFit

We further performed a similar statistical study to test the excess of X-ray emission with respect to the off-axis structured jet light-curves modeled with JetFit (Duffell & MacFadyen 2013; Ryan et al. 2015; Wu & MacFadyen 2018). JetFit fits the afterglow light curves for arbitrary viewing angles using a ‘boosted-fireball’ structured jet model to compute the jet dynamics as it spreads. It naturally accommodates a diverse range of outflows from mildly-relativistic quasi-spherical outflows to ultra-relativistic highly collimated jets. JetFit uses the python package `emcee` to explore the full parameter space formed by eight parameters: the explosion energy, $E_{\text{B}}$; the ambient density, $n$; the asymptotic Lorentz factor, $\eta_B$; the boost Lorentz factor, $\gamma_B$; the spectral index of the electron distribution, $\gamma$; the electron energy fraction, $\epsilon_e$; the magnetic energy fraction, $\epsilon_B$; and viewing angle $\theta_{\text{obs}}$; and finds the best-fitting values and their posterior distributions. Because the broadband SED (spectral energy distribution) of GW 170817, from $\delta t = 2 − 745$ days, is best explained by a simple power-law, some of these parameters are highly degenerate and the problem is under-constrained. Hence, we fixed $\epsilon_e = 0.1$, as predicted from the simulations of particle acceleration by relativistic shocks (Sironi et al. 2013), $n = 0.01 \text{cm}^{-3}$, the upper-limit on the ambient density inferred from the study of the host X-ray thermal emission (Hajela et al. 2019), and we computed the best-fitting models assuming three values of $\gamma_B = 7, 10, \text{and } 12$. We selected these $\gamma_B$ values based on the VLBI measurements of the angular displacement of the radio emission with time, which constrained the jet Lorentz factor $\Gamma \approx 4$ at the time of the afterglow peak (or $\theta_{\text{obs}} − \theta_j \approx 1/\Gamma \approx 1/4$, Mooley et al. 2018a).4 We use JetFit to fit the multi-wavelength afterglow light-curves at 3 GHz, 6 GHz, optical and at 1 keV frequencies acquired at $2 < \delta t < 900$ days. The jet opening angle $\theta_j$ of GW 170817 has been estimated to be of the order of a few degrees (Mooley et al. 2018a; Ghirlanda et al. 2019; Nathanael et al. 2021), and we thus consider the $\gamma_B = 12$ boosted fireball model as our fiducial case. The best-fitting light curves for the $\gamma_B = 12$ are shown in Figure 4, while the one- and two-dimensional projections of the posterior distribution of the free parameters for $\gamma_B = 12$ are provided in Appendix B, Figure 13.

We use the full posterior distribution of all the free parameters to compute the distribution of flux density at 1 keV at $t_1$ and $t_2$ for each choice of $\gamma_B$. Similar to the above statistical analysis, we convert these flux densities to the total counts in the 0.5–8 keV energy range in a $1''$ region, calculate the

Probabilities in the form of % added as per Reference Request.
probability of each sample, $i$, $P_{ij} = \text{Pois}(c \geq N_{\text{obs},ij}|c_i)$, where $j \in 1, 2$ for the two epochs respectively, and finally compute the cumulative probabilities, $P_i$, to lead to a deviation at least as prominent as the one observed at $t_1$ (bottom panel, Figure 3). For different values of $\gamma_B$, we find $P_1$ in the range $P_1 = 0.07 - 0.15$ and $P_2 = 7.36 \times 10^{-4} - 2.82 \times 10^{-5}$, corresponding to a $2.9\sigma - 3.4\sigma$ (Gaussian equivalent, $99.6268\% - 99.9326\%$) deviation of the observed X-rays at 1234 days from the light-curve modeled by the off-axis structured jet model. We further find $P_1 \times P_2 = 5.59 \times 10^{-6} - 4.69 \times 10^{-4} (3.5\sigma - 4.0\sigma$ Gaussian equivalent, $99.9535\% - 99.9937\%)$, and $P_{\text{combined}} = 2.62 \times 10^{-4} - 2.10 \times 10^{-3} (3.1\sigma - 3.7\sigma$, where the range reflects the assumed values of $\gamma_B$ used) to obtain deviations from the off-axis structured jet model at least as prominent as those observed at both epochs $t_1$ and $t_2$. Larger $\gamma_B$ values imply a higher level of collimation of the jet, and hence a faster post-peak transition to the asymptotic power-law decay, which explains the highest significance of the excess associated to the $\gamma_B = 12$ model (bottom panel, Figure 3). Since for GW 170817 $\theta_2 \leq 5^\circ$ (e.g., Mooley et al. 2018a; Ghirlanda et al. 2019) and our most collimated model has $\gamma_B = 12$ (i.e. $\theta_2 \approx 5^\circ$), in this sense the probabilities derived with this approach are conservative. For the same reason, $\gamma_B = 12$ is our baseline model and for this set of models the probabilities associated with $\gamma_B = 12$ should be considered the most realistic estimates (i.e. $P$ of chance deviation corresponding to $3.7\sigma$). The chance probabilities as a function of $\gamma_B$ are reported in Table 3.

From Figure, right panel, 3, the $\gamma_B = 12$ best fitting model lies slightly above the central value of the data points at $\delta t > 300$ days, but it is well within the $1\sigma$ error bars of the data at $\delta t > 600$ days and always within the $2\sigma$ range. For this model the $\chi^2/dof = 1.03$. We further tested the departure from a random distribution of the signs of the residuals implementing a Runs test for randomness. Our data set contains 54 data points and the number of runs is 24. The chance probability of obtaining the observed distribution of runs is $26\%$. It follows that the hypothesis of random distribution of the model’s residuals cannot be rejected.

4.3. General Considerations

Both statistical approaches detailed above (i.e. the jet afterglow light-curve models and the universal post jet-break power-law decay) independently lead to the conclusion of the presence of an X-ray excess of emission at $\delta t > 900$ days with statistical confidence $\geq 3.1\sigma$. Observations acquired around 940 days alone do not provide any statistically significant evidence of a deviation from the expectations of an off-axis jet model as we reported in Hajela et al. (2020) (see also Troja et al. 2020). The statistical significance of the excess of X-ray emission is driven by our most recent epoch of CVO data at 1234 days. We also note that we do not claim a re-brightening of the X-ray flux, but a statistically significant deviation from the existing models that best fit the afterglow at $< 900$ days, which points to the emergence of a new X-ray component. Our approach is agnostic with regard to the spectral and temporal properties of any additional emission component. The statistical tests that we carried out have been explicitly designed to avoid any dependency on any assumed property of the additional component and instead test for a deviation compared to expectations from the jet afterglow emission.

We note that systematic uncertainties on the relative flux calibration of Chandra/ACIS-S between observations acquired at $\delta t < 900$ days and $\delta t > 900$ days have minimal impact on our conclusions. We use the JetFit models with $\gamma_B = 12$ here as an example to quantify this effect. Specifically, adopting a systematic RMS flux variation of $< 3.4\%$ (Chandra calibration team, private communication) on Chandra/ACIS-S fluxes, and assuming that fluxes at $\delta t > 900$ days have been systematically overestimated by that RMS factor, we find evidence for a $3.97\sigma$ (Gaussian equivalent) deviation of the X-rays emission at $\delta t > 900$ days from the best fitting model. Similar results hold for the universal post-jet break afterglow models. Finally, we note that correcting or not correcting for PSF-losses the count-rates at $\delta t > 900$ days induces changes in the stated statistical significances of the excess of $\lesssim 0.1\sigma$ (Gaussian equivalent), demonstrating that the choice of the aperture size of $15^\prime$ does not drive our conclusions.

We end by addressing the difference between our conclusions and the claim of a statistical significance of the X-ray excess of $\lesssim 3\sigma$ that appeared in Troja et al. (2021). The main source of difference between our analysis and the one presented in Troja et al. (2021), which drives the different conclusions about the statistical evidence for an X-ray excess, is related to the statistical treatment of the data, to the Poisson nature of the X-ray signal at $t > 900$ days, and to the specific jet model chosen as a reference. Specifically, the use of a jet model presented in their work that is not in tension with the VLBI measurements would have led to the inference of a significantly larger discrepancy between X-ray observations at $\delta t > 900$ days and expectations as we demonstrate in Figure 12 in Appendix A. The X-ray flux calibration plays a negligible statistical role, as we show in Figure 12 and Appendix A. Our statistical tests self-consistently account for the Poisson nature of the process, using jet models that are not in violation of the VLBI constraints. To the extent of the authors’ knowledge, there is no jet model that does not violate the VLBI constraints and can naturally reproduce the late time X-rays of GW 170817.

5. INFERENCES ON THE BROADBAND SPECTRUM AT 1234 DAYS

The broadband X-ray-to-radio non-thermal emission from the jet afterglow of GW 170817 at $\delta t < 900$ days is well fitted by a simple power-law spectral model $F_\nu \propto \nu^{-\beta}$ with $\beta = 0.583 \pm 0.013$ (Fong et al. 2019), or equivalently, $F_\nu \propto \nu^{-(p-1)/2}$ with $p = 2.166 \pm 0.026$ in the optically thin synchrotron regime. In this section we compute the constraints on the spectral slope at $= 1234$ days that are imposed by the X-ray detection ($\S 2$) and the 3 GHz radio limits ($\S 3.1$) under the assumption that the broadband spectrum is still de-
Figure 4. Left Panel: Non-thermal emission from GW 170817 across the electromagnetic spectrum and best fitting universal post jet-break model, as explained in §4, with $t_{\text{start}} = 196$ days. Right Panel: Non-thermal emission from GW 170817 and best fitting jet-afterglow model computed with JetFit for $n = 0.01$ cm$^{-3}$, $\epsilon_e = 0.1$, and $\gamma_B = 12$ fixed. In both panels empty symbols were not included in the fitting procedure but are shown here for completeness adopting a flux calibration consistent with the afterglow models. Colored bands identify the 68% flux confidence interval. The grey empty square symbol is the peak pixel value within one synthesized beam at the location of GW 170817 at 3 GHz from Balasubramanian et al. 2021. The bottom subplots show the difference between observations and the best-fitting models as derived from the model posteriors, and expressed in units of $1\sigma$ data uncertainties for displaying purposes.

scribed by a simple power-law model. Radio limits at 15 GHz and 0.8 GHz (§3.1-3.2), and HST observations (Kilpatrick et al. 2021) do not provide additional constraints on the simple power-law model (Figure 5). We used MCMC sampling within Xspec as described in §2.2 and we sampled 10$^6$ times the posterior probability distribution of the unabsorbed 0.3 – 10 keV flux derived from fitting the CXO data at 1234 days employing Cash-statistics. This method accounts for deviations from Gaussian statistics that manifest in the regime of low spectral counts. We then computed as a function of $p$ the probability associated with spectral models $F_\nu \propto \nu^{-(p-1)/2}$ that would not lead to a radio detection, here defined as a 3 GHz radio flux density above 3 ×, or alternatively 2 ×, the flux density root mean square – RMS – of our image around the location of GW 170817, where RMS $= 1.7 \mu$Jy.

Our results are shown in Figure 6. We find that values of $p > 2.166$, i.e. larger than the best fitting value of the jet-afterglow at $\delta t < 900$ days are ruled out with statistical confidence $\geq 92\% - 99.2\%$. These results suggest the evolution of the broadband spectrum towards lower values of $p$ and constitute the first indication of spectral evolution of the non-thermal emission from GW 170817. This conclusion is strengthened by using the RMS $= 1.3 \mu$Jy at 3 GHz from Balasubramanian et al. 2021. We end by noting that HST observations acquired on $\delta t = 1236.5$ days since merger at $\nu = 2.13 \times 10^{14}$ Hz (Kilpatrick et al. 2021) imply an optical to X-ray spectral index $\beta_{OX} \lesssim 0.97$ (where $F_\nu \propto \nu^{-\beta_{OX}}$). Finally, our VLA observations at 15 GHz reach a similar depth as our 3 GHz observations and rule out an optically thick $F_\nu \propto \nu^2$ radio source with flux density $F_\nu \geq 0.06 \mu$Jy at $\nu = 3$ GHz.

6. LATE TIME EVOLUTION OF THE EMISSION FROM OFF-AXIS JET AFTERGLOWS

In the context of synchrotron emission from an ultra-relativistic off-axis jet, a post-peak late-time flattening of the light-curve can be the result of: (i) the jet encounter with an over-density in the environment; (ii) energy injection; (iii) time-varying shock microphysical parameters $\epsilon_B$ and $\epsilon_e$; (iv) transition into the sub-relativistic phase; and (v) emergence of the counter-jet emission (Granot et al. 2018; Nakar & Piran 2021).

The universal post jet-break light-curve evolution for an observed frequency $\nu$ above the synchrotron self-absorption frequency $\nu_{\text{sh}}$ and for $\nu_m < \nu < \nu_c$ (where $\nu_m$ is the synchrotron frequency and $\nu_c$ is the cooling frequency) is (Gra-
probability of simple power-law $F_{\nu} = \text{Norm} \times \nu^{-(p-1)/2}$ spectral models at 1234 days that do not violate the $3\times\text{RMS}$ (orange), and $2\times\text{RMS}$ (brown) flux density of our 3 GHz image at the location of GW 170817 as a function of $p$, where RMS=1.7 $\mu$Jy inferred from this work. Red line and open symbols: results for RMS=1.3 $\mu$Jy inferred by Balasubramanian et al. 2021.  

$\text{Norm}$ is drawn from the posterior probability distribution of the 0.3 – 10 keV unabsorbed X-ray flux at 1234 days as derived from MCMC sampling within $\text{Xspec}$. Horizontal blue dashed lines mark the 0.3%, 4.5% and 50% probability levels. Vertical blue thick and dotted lines: best fitting $p$ parameter and 1 $\sigma$ range for the jet afterglow as derived from broad-band SED fitting of the non-thermal emission of GW 170817 at $\Delta t < 900$ days (Fong et al. 2019). This analysis suggests a hardening of the non-thermal spectrum of GW 170817 at 1234 days to values of $p < 1$ than the best-fitting value from the earlier jet afterglow at statistical confidence $\gtrsim 92\% – 99.2\%$.

GC might otherwise provide a physical reason for an abrupt change in the external gas density on the scale probed by the afterglow. We thus do not consider the over-density scenario any further.

Following a similar line of reasoning, an excess of emission can be produced if the shock is re-freshed by the deposition of new energy (e.g. Laskar et al. 2015; Sari & Mészáros 2000). From Eq. 1, a flux ratio of $\approx 4$ requires the late-time deposition of a large amount of additional energy similar to the jet energy $E_k$. There is no plausible energy source that can power the sudden energy release of an amount of energy equivalent to the jet energy at late times and we consider this scenario unlikely. Finally, a sharp variation of the shock microphysical parameters $\epsilon_e$ and $\epsilon_B$ with time can in principle lead to larger fluxes. This scenario would require an ad hoc evolution of $\epsilon_e$ and $\epsilon_B$ to explain the X-ray observations and we thus consider this model not physically motivated. Additionally, the deceleration of the shock is expected to lead to smaller $\epsilon_e$ values, while larger $\epsilon_e$ values would be needed to explain a flatter light-curve. In addition to the arguments above, we end by noting that all the models discussed so far do not naturally explain the harder radio-to-X-ray spectrum with a reduced value of $p$ (§5).
In the absence of energy injection, environment over-densities and variations in the shock microphysical parameters, the transition of the blast wave dynamics to the sub-relativistic phase at \( t_{\text{NR}} \approx 1100(E_{\text{k,in},53}/n)^{1/3} \) days (Piran 2004) is expected to lead to a smooth transition to a less steeply decaying light-curve \( F_\nu \propto t^{-(p-1)/2+3/5} \) at \( \nu < \nu_m \) (Equation 97, Piran 2004) or \( F_\nu \propto t^{-(p-1)/2+1/2} \) at \( \nu > \nu_c \) (equation A20, Frail et al. 2000). For \( p = 2.05 - 2.15 \) we expect the light-curve to decay as \( F_\nu \propto t^{-1.2 - 2 \times 10^{-9}} \) in the non-relativistic regime. For the jet-environment parameters of GW 170817 (Mooley et al. 2018a; Hotokezaka et al. 2019; Ghirlanda et al. 2019; Ryan et al. 2020, Figure 4) the full transition to the non-relativistic regime and the appearance of the counter jet is expected at \( t_{\text{NR}} \ge 5000 \) days, significantly later than our current epoch of observation, with the start of the “deep Newtonian phase” being at even later times. In the deep Newtonian phase \( F_\nu \propto t^{-(1+p)/10} \) or \( F_\nu \propto t^{-0.9} \) for \( p = 2.05 - 2.15 \) (Sironi & Giannios 2013). A smooth transition to the sub-relativistic regime, accompanied by a slower light-curve decay, might start to be noticeable at earlier epochs, and possibly now, as the jet-core bulk Lorentz factor is \( \Gamma(t) \approx 4(t/100 \text{ days})^{-3/8} \) at the current epoch (still in the Blandford-McKee regime, no jet spreading) or \( \Gamma(t) \propto t^{-1/2} \) leading to \( \Gamma(t) \approx 1.1 \) for exponential jet spreading (Rhoads 1999). These estimates are based on the inferred \( \Gamma \approx 4 \) at \( \approx 100 \) days (Mooley et al. 2018a). In both cases the light-curve evolution is expected to be achronic and the emission is expected to become dimmer with time as \( F_\nu \propto t^{-1} \) or steeper. No excess can be explained within the non-relativistic jet transition scenario and no spectral evolution is expected unless we invoke an ad hoc temporal evolution of \( p \) from \( p = 2.15 \) to \( p = 2.0 \) in the time range \( 900-1200 \) days (i.e. well before the full transition to the non-relativistic phase) as the shock decelerates. The theoretical predictions from the Fermi process of particle acceleration in shocks would support this trend of evolution, as they predict \( p = 2 \) at non-relativistic shock speeds (Bell 1978; Blandford & Ostriker 1978; Blandford & Eichler 1987) and \( p \approx 2.22 \) at ultra-relativistic velocities in the test particle limit (Kirk et al. 2000; Achterberg et al. 2001; Keshet & Waxman 2005; Sironi et al. 2013). However, here the challenge is represented by having a shock where the index of the non-thermal electron distribution \( p \) changes with time as a result of the shock deceleration, without having a substantial drop in the electron acceleration efficiency \( \epsilon_e \) when compared to the earlier ultra-relativistic regime (Crumley et al. 2019). Finally, the emergence of the counter-jet emission is expected to lead to a flatter light-curve at \( \Delta t > t_{\text{NR}} \), or \( \Delta t > 5000 \) days for the parameters of GW 170817.

To summarize, the late time evolution of the jet does not naturally account for the brightness, spectrum and flattening of the X-ray light-curve at \( \Delta t \approx 1200 \) days. Specifically: (i) the steep density gradient of a factor of \( \approx 10^5 \) over a pc scale required to explain the X-ray excess of emission implies an extremely large shell mass \( \ge 10 M_\odot \) within the jet angle at \( \approx 1 \) pc, making the scenario of a jet encounter with the edge of an associated pulsar-wind bubble unlikely; (ii) similarly, the large amount of energy required to be injected to produce a X-ray excess is equivalent to the energy of the jet itself and there is no plausible source to power such an energy release at these late-times; (iii) a sudden variation of the shock microphysical parameters is not physically motivated at this epoch; (iv) the shock transition to the Newtonian regime is expected to happen at significantly later times \( t_{\text{NR}} \ge 5000 \) days and no effect related to the Newtonian transition can thus be invoked to explain the late-time excess of X-ray emission; (v) lastly, the counter-jet is also expected to emerge at \( \Delta t > 5000 \) days.

7. KILONOVA AFTERGLOW MODELS AND NUMERICAL RELATIVITY SIMULATIONS OF BNS MERGERS

NS merger simulations predict the ejection of neutron-rich and neutron-poor matter due to a variety of mechanisms operating over different timescales before, during and after the merger (Shibata & Hotokezaka 2019). These mass outflows shock the circumbinary medium producing synchrotron radiation that peaks on the deceleration time scale \( t_{\text{dec}} \) (Nakar & Piran 2011). The direct implication is that heavier mass outflows like those associated with the kilonova ejecta will produce non-thermal emission that will peak later in time than the emission associated with the significantly faster but also significantly lighter jet. For the inferred kilonova ejecta properties of GW 170817 \( (M_{\text{ej}} \approx 0.06 M_\odot, n \approx 0.01 - 0.001 \text{ cm}^{-3} \text{ and } \beta \approx 0.1 - 0.3 \text{; Villar et al. 2017; Cowperthwaite et al. 2017; Arcavi 2018; Waxman et al. 2018; Nicholl et al. 2021; Bulla et al. 2019; Drout et al. 2017; Kilpatrick et al. 2017}), t_{\text{dec}} \approx 10^4 \text{ days}. However, the deceleration of the fastest-moving tail of these ejecta is expected to contribute to non-thermal emission on significantly shorter timescales of months to years after the merger (Nakar & Piran 2011; Kyutoku et al. 2014; Takami et al. 2014; Hotokezaka & Piran 2015; Hotokezaka et al. 2018; Kathirgamaraju et al. 2019; Margalit & Piran 2020) that are relevant now (while the bulk of slower-moving ejecta powered the UV/optical/IR kilonova at \( \Delta t < 70 \) days).

This kilonova afterglow will appear as an excess of emission compared to the off-axis jet afterglow. Being powered by a different shock and by a different electron population than the jet’s forward shock, the synchrotron emission from the kilonova afterglow does not necessarily inherit the same microphysical parameters \( \epsilon_e, \epsilon_B \), as well as the electron index \( p \). In this respect, the lower \( p \) value indicated by our observations (Figure 6) would be a natural outcome and would be consistent with the \( p < 2.2 \) theoretical expectation of shocks that are non-relativistic (Bell 1978; Blandford & Ostriker 1978; Blandford & Eichler 1987).

The luminosity and time evolution of the kilonova afterglow from a BNS merger depends on (and is a tracer of) the intrinsic parameters that include how the ejecta energy is partitioned in the velocity space \( E_{\text{CN}}(\Gamma, \beta) \), which ultimately depends on the neutron star equation of state (EoS) and the binary mass ratio \( q \), and also the extrinsic parameters that include those that regulate the kilonova shock microphysics (fraction of post-shock energy density in relativistic
electrons, $\epsilon_{e,KN}$, and in magnetic field, $\epsilon_{B,KN}$ and $p_{KN}$), and the environment density $n$. We first adopt in §7.1 an analytical parametrization of $E_{KN}(\Gamma \beta)$ to explore the large parameter space of the kilonova afterglow parameters while being agnostic to the ejecta type (e.g., winds vs. dynamical etc.). In the second part (§7.2) we employ a set of numerical relativity simulations of BNS mergers to emphasize the dependency of the observed kilonova afterglow on intrinsic parameters of the NS binary, like the binary mass ratio or the NS EoS. We note that the potential early emergence of the kilonova afterglow a few years after the merger, at a time when the jet has yet to effectively become spherical (§6) implies that the kilonova shock is expanding into a medium that is mostly unperturbed (i.e., not shocked by the jet shock) and that effects related to the jet evacuating the circum-merger medium (Margalit & Piran 2020) are unlikely to play a major role.

7.1. Kilonova afterglow models from Kathirgamaraju et al. 2019

We parameterized the kinetic energy distribution of the kilonova ejecta as a power-law in specific momentum $\Gamma \beta$ for $\beta > \beta_0$: $E_{KN} \propto (\Gamma \beta)^{-\alpha}$ (Kathirgamaraju et al. 2019). This parameterization captures the properties of the high-velocity tail of all types of kilonova outflows, including dynamical ejecta and disk winds that might dominate the mass of the blue kilonova component. Motivated by the results from the modeling of the thermal emission from the kilonova in the following we adopt $\beta_0 = 0.35$ as baseline and a total kinetic energy of $E_{KN}(\Gamma \beta \beta_0) = 10^{51}$ erg. We generated a set of multi-wavelength kilonova afterglow light-curves for shock microphysical parameters $p = 2.05$ (consistent with the observational findings of §5), $\epsilon_e = 0.1$, $\epsilon_B = [10^{-4} - 10^{-2}]$ and circumbinary medium density $n = [10^{-4} - 10^{-2}]$ cm$^{-3}$. As a comparison, studies of the jet afterglow pointed at densities $n > 10^{-3}$ cm$^{-3}$ (Margutti & Chornock 2021), while multiple studies (Hallinan et al. 2017; Hajela et al. 2019; Makhatthini et al. 2020) of the large-scale environment of GW 170817 at X-ray and radio wavelengths argue in favor of $n \leq 10^{-2}$ cm$^{-3}$. Motivated by the results from numerical relativity simulations of BNS mergers described below we explore the parameter space for $\alpha = [3 - 9]$.

Our results are shown in Figure 7, where shaded areas highlight the regions of the parameter space that are consistent with the bright X-ray excess (blue) and the deep radio upper limit (orange). We further show a successful kilonova afterglow model for $\alpha = 5$, $n = 0.001$ cm$^{-3}$ and $\epsilon_B = 0.001$ in Figure 2. Consistent with the results from the jet afterglow modeling, current data point to lower density environments with $n < 0.01$ cm$^{-3}$, but otherwise leave the multidimensional parameter space largely unconstrained. Specifically, we find that all values of $\alpha = [3, 10]$ are consistent with the X-ray and radio data set. This conclusion remains unchanged even if we adopt the peak pixel flux within one synthesized beam at 3 GHz from Balasubramanian et al. (2021) ($F_v = 2.8 \pm 1.3 \mu Jy$) as a constraint on the radio emission from the kilonova (Figure 8).

Using their reduction of the multi-wavelength data set up to $\approx 1200$ days and similar to our preliminary assessment of the properties of the kilonova ejecta properties in Hajela et al. (2019), Balasubramanian et al. (2021) favor $\alpha \geq 5$ kilonova ejecta profiles assuming a density and the kilonova shock microphysical parameters set to the values of the jet afterglow shock (i.e. $n \sim 10^{-2}$ cm$^{-3}$, $\epsilon_e \sim 10^{-2}$, and $\epsilon_B \sim 10^{-3}$). While for this choice of extrinsic parameters our findings qualitatively agree with the conclusions by Balasubramanian et al. (2021), we note that there is no physical reason for the kilonova shock microphysical parameters to be the same as those of the jet afterglow shock, and relaxing these parameters leaves the problem unconstrained. Our results are consistent with those from previous analyses that did not include the latest epoch (Hajela et al. 2019; Troja et al. 2020), and constitute an important advancement with respect to these previous works that were completed before the emergence of a statistically significant new component of emission.

7.2. Kilonova afterglows from physically-motivated kilonova kinetic energy profiles

We consider a set of 76 numerical relativity BNS merger simulations tailored to GW 170817 (Perego et al. 2019; Endrizzi et al. 2020; Nedora et al. 2019; Bernuzzi et al. 2020; Perego et al. 2020; Nedora et al. 2021b). The simulations were performed using the WhiskyTHC code (Radice & Rezzolla 2012; Radice et al. 2014a,b). The set includes simulations performed at different resolutions and employs five finite-temperature microphysical equations of state (EoSs) that span the (large) range of EoS compatible with current laboratory and astronomical constraints. The simulations self-consistently included compositional and thermal effects due to neutrino emission and re-absorption (Radice et al. 2016, 2018c). The general-relativistic large-eddy simulation (GRLES) method was used to capture subgrid-scale turbulent dissipation and angular momentum transport (Radice 2017, 2020).

Dynamical ejecta from these simulations show the presence of a fast moving tail of ejecta, which is produced following the centrifugal bounce of the remnant taking place in the first milliseconds of the merger, unless prompt BH formation occurs, in which case there is no bounce (Radice et al. 2018c). The bounce produces a shock wave that is rapidly accelerated by the steep density gradient in the outer layers of the remnant, propels material to trans-relativistic velocities, and propagates into the circumbinary medium. Fast moving material could also be accelerated by the thermalization of mass exchange flows between the stars prior to merger (Radice et al. 2018b). However, this alternative scenario typically predicts a faster rise of the synchrotron emission than indicated by observations of GW 170817.

The deceleration of this kilonova shock into the medium produces synchrotron radiation. We compute the kilonova synchrotron light curves using the semi-analytic code PyBlastAfterglow (Nedora et al. 2021a). We have validated this code in the subrelativistic regime by comparing the results it produces using the ejecta profiles from Radice et al.
Figure 7. Blue shaded area: region of the parameter space consistent with the X-ray flux excess at 1234 days following the modeling described in §7. Orange shaded area: region of the parameter space that is consistent with our radio upper limit at 3 GHz: $F_\nu < 5.1 \mu$Jy. The kinetic energy distribution of the kilonova ejecta in the velocity space has been parameterized as $E_{\text{KN}} \propto (\Gamma \beta)^{-\alpha}$ above $\beta_0$ with $E_{\text{KN}}(\Gamma_0 \beta_0) = 10^{51}$ erg. The shock microphysical parameters adopted in this calculation are $p = 2.05$ (consistent with the observational findings of §5) and $\epsilon_e = 0.1$. Two parameters are varied in each plot while the rest are kept fixed to values indicated in the plot title.

Figure 9 collects a representative set of X-ray light curves for three EoSs (BLh, Logoteta et al. 2021; Bernuzzi et al. 2020; LS220, Lattimer & Swesty 1991; and SLy4, Douchin & Haensel 2001; Schneider et al. 2017) and two values of the binary mass ratio $q$. This figure highlights the sensitivity of the kilonova afterglow on intrinsic (EoS, $q$) and extrinsic ($n$, $p$, $\epsilon_e$, $\epsilon_B$) parameters of the binary. It is important to emphasize that the overall flux level predicted by our models is strongly dependent on assumed microphysical parameters of the shock. However, the light curve temporal evolution only depends on the structure of the ejecta and on the ISM density. Specifically, the peak time of the kilonova emission is of dynamical nature, tracing the deceleration time of the blast wave into the environment (Nakar & Piran 2011) and it is thus independent from the parameters that set the level of the emitted flux (like the shock microphysical parameters).

With respect to the intrinsic binary parameters probed by our simulation, we find that binaries which do not undergo prompt BH formation are broadly consistent with the observations. Numerical simulations of BNS mergers by Prakash et al. (2021); Nedora et al. (2021a) show that if prompt collapse to BH occurs in equal mass NS binaries, the kilonova afterglow is expected to be several orders of magnitude fainter than the observed X-ray luminosity of GW 170817 at $\approx 1000$ days (e.g. Figure 15 in Prakash et al. 2021). In the case of highly asymmetric NS binaries, the prompt collapse to BH is associated with afterglow light curves that peak at $\approx 10^4$ days post-merger, which is significantly later than the
current epoch (see Figure 4 and 5 in Nedora et al. 2021a). An important conclusion is that prompt BH formation is disfavored (Bauswein et al. 2017; Margalit & Metzger 2017; Radice et al. 2018d), because the presence of the post-merger bounce appears to be necessary in order to produce sufficient fast and massive outflows to power the kilonova emission. Improved higher-resolution targeted simulations are needed to draw more quantitative conclusions.

In addition to the nature of the compact-object remnant, the early detection of a kilonova afterglow a few years after the merger and its future modeling can enable fundamental insight into two other still-open questions pertaining to GW 170817: the presence of a free-neutron component of ejecta, and the origin of the detected prompt $\gamma$-rays (Goldstein et al. 2017; Savchenko et al. 2017). Fast ejecta with mass $\gtrsim 10^{-4} M_\odot$ at velocity $v \gtrsim 0.5c$ (light-blue shaded area in Figure 10, lower panel) are expected to lead to a freeze out of the $\tau$-process (Metzger et al. 2015), as most neutrons will avoid capture, leaving behind free neutrons that can power a short-lived (i.e. $\approx$ hrs) but luminous UV/optical transient. Additionally, kilonova ejecta profiles extending to velocities $v \geq 0.6c$ (light-green shaded area in Figure 10, lower panel) provide the necessary conditions to produce $\gamma$-rays from a shock breakout of a wide-angle outflow (i.e. the cocoon) inflated by the jet from the merger ejecta (Bromberg et al. 2018; Gottlieb et al. 2018). Being sensitive to the presence and properties of the fast kilonova ejecta, the kilonova afterglow is thus a probe of the merger dynamics and nature of the compact object remnant.

We conclude by remarking that a general, robust and testable prediction of the kilonova afterglow models is that of a persistent source of emission across the electromagnetic spectrum, which is not expected to become fainter for thousands of days, and might even become brighter during this period of time. Eventually, the kilonova afterglow will appear as a detectable source in the radio sky and might even be detectable via deep optical observations from space.

8. EMISSION FROM A COMPACT-OBJECT REMNANT

An alternative explanation of rising X-rays without accompanying bright radio emission is that of central-engine powered radiation, i.e. radiation powered by an energy release associated with the compact-object remnant either in the form of accretion (for a BH remnant) or spin-down energy (for a long-lived NS remnant). The nature of the compact-object remnant of GW 170817 is a fundamentally open question that directly relates to the NS EoS. While post-merger GWs were inconclusive, the observational evidence for (i) a blue kilonova component associated with a large mass of lanthanide-free ejecta and kinetic energy $\approx 10^{51}$ erg (Evans et al. 2017; Villar et al. 2017; Cowperthwaite et al. 2017; Nicholl et al. 2021; Bulla et al. 2019), and (ii) the uncontroversial evidence for a successful relativistic jet (Alexander et al. 2018; Mooley et al. 2018a; Ghirlanda et al. 2019) together with energetics arguments strongly disfavor either a prompt collapse to a BH or a long-lived NS remnant. These arguments and observations argue in favor of a hypermassive NS that collapsed to a BH within a second or so after the merger (Granot et al. 2017; Margalit & Metzger 2017; Shibata et al. 2017; Metzger et al. 2018; Rezzolla et al. 2018; Gill et al. 2019; Ciolfi 2020; Murgua-Berthier et al. 2021). While the most likely scenario is that of a BH remnant at the current time of the observations, in the following we also consider the less-likely case of a spinning-down NS for completeness (see however Piro et al. 2019).

8.1. Accreting BH remnant scenario

The Eddington luminosity for accretion onto a remnant BH of mass $M_\bullet \sim 2.5 M_\odot$ (Abbott et al. 2019) of GW 170817 is given by

$$L_{\text{Edd}} = \frac{4\pi GM_\bullet c}{\kappa_{\text{es}}} \approx 8 \times 10^{38} \left(\frac{M_\bullet}{2.5 M_\odot}\right) \text{erg s}^{-1},$$

(2)
where $\kappa_{ee} = Y_e \sigma_T / m_p \approx 0.16 \text{ cm}^2 \text{ g}^{-1}$ is the approximate electron scattering opacity for fully ionized matter comprised of heavy elements (electron fraction $Y_e \approx 0.4$).

From hydrodynamical simulations of BNS mergers, the rate of fall-back accretion is $M_{\text{t}} \sim 2 \times 10^{-4} M_\odot \text{ s}^{-1}$ on a timescale of $t_0 \sim 1 \text{ s}$ after the merger (Rosswog 2007). A more important source of fall-back material may arise from the accretion disk outflows (Fernández & Metzger 2013), which likely dominated the kilonova ejecta in GW 170817 (Radice et al. 2020). If a few tens of percent of the total ejecta mass $\approx 0.06 M_\odot$ inferred for GW 170817 (Villar et al. 2017; Cowperthwaite et al. 2017; Nicholl et al. 2021; Arcavi 2018; Waxman et al. 2018) were to fall back to the BH on a timescale comparable to the predicted accretion disk lifetime $\sim 1 \text{ s}$, the mass fall-back rate would be orders of magnitude higher, $M_{\text{t}} \sim 10^{-2} M_\odot \text{ s}^{-1}$.

Based on the expectation that $\dot{M} \approx \dot{M}_{\text{t}} (t/t_0)^{-5/3}$ at times $t \gg t_0$ for marginally bound material (Rees 1988), the total X-ray accretion luminosity is given by

$$L_X \approx \frac{\eta}{f_b} \frac{\dot{M}}{c_3} \approx 10^{39} \text{ erg s}^{-1} \left( \frac{f_b}{0.1} \right)^{-1} \times \left( \frac{\eta}{0.1} \right) \left( \frac{\dot{M}_{\text{t}}}{10^{-2} M_\odot \text{ s}^{-1}} \right) \left( \frac{t}{1000 \text{ days}} \right)^{-5/3}$$

(3)

where the radiative efficiency $\eta$ has been normalized to that of a thin disk orbiting a BH of dimensionless spin $a \approx 0.6 - 0.8$ (Novikov & Thorne 1973), as expected for the remnant of a BNS merger. Here $f_b$ is the geometric beam-
Figure 10. Upper Panel: Colored lines: kinetic energy profile of the fastest kilonova ejecta as a function of specific momentum $\Gamma \beta$. Dark-red to orange shade: dynamical ejecta profiles as inferred from ab-initio numerical-relativity simulations described in §7 for different EoS and NS mass ratios $q$. Blue lines: $E_{\text{KN}}(>\Gamma \beta) \propto (\Gamma \beta)^{-\alpha}$ analytical profiles that include the contributions from all types of kilonova ejecta for $\alpha = 4, 5, 6, 7, 9$. Black filled circles: kinetic energy inferred from the modeling of the UV/optical/NIR kilonova emission (Villar et al. 2017). Grey squares: SGRB jets (Wu & MacFadyen 2019). Lower Panel: kilonova ejecta profiles in the mass phase-space. Green colored area: region of the parameter space consistent with a cocoon shock breakout origin of GRB 170817A (Gottlieb et al. 2018). Blue colored area: region of the parameter space which is suggestive of a free-neutron component of the ejecta expected to power a short-lived UV/optical transient.
the maximum of two timescales. The first is the timescale for the accretion rate to drop sufficiently that the beaming fraction $f_b \propto (M/M_{Edd})^{-2} \propto t^{10/3}$ (King 2009) increases to the point that the angle of the accretion funnel $\theta_b \propto f_b^{1/2} \propto t^{5/3}$ enters the observer’s viewing angle $\theta_{obs} \approx 0.4$. Given that $L_X$ at the present epoch is $\lesssim L_{Edd}$ (Eq. 2), we conclude that this effect may still play a role in generating a rising X-ray luminosity.

A second timescale for the X-rays to be able to reach the observer is that required for the kilonova ejecta to become transparent to the X-rays. Assuming that the $r$-process ejecta have a bound-free opacity to photons of energy $\sim 1$ keV which is similar to that of iron group elements $\kappa_X \approx 10^4$ cm$^{-2}$ g$^{-1}$, this will take place after a time

$$t_{thin} = \left( \frac{3M_{ej}\kappa_X}{4\pi v_{ej}} \right)^{1/2} \approx 2000 \text{ days} \left( \frac{v_{ej}}{0.1c} \right)^{-1} \times \left( \frac{\kappa_X}{10^4 \text{ cm}^2 \text{ g}^{-1}} \right)^{1/2} \left( \frac{M_{ej}}{0.06M_\odot} \right)^{1/2}, \quad (6)$$

where we have normalized the ejecta mass $M_{ej}$ and velocity $v_{ej}$ to characteristic values for the (dominant) red/purple ejecta component inferred by modeling the optical/IR kilonova of GW 170817 (Villar et al. 2017; Cowperthwaite et al. 2017; Drout et al. 2017; Kilpatrick et al. 2017).

Given that the ejecta density may be lower than average for our high altitude viewing angle $\theta_{obs} \approx 0.4$, and hence $t_{thin}$ somewhat over-estimated, we conclude that $t_{thin}$ is also likely to be comparable to the present epoch. Figure 11 shows the evolution of the accretion-powered fall-back X-ray luminosity on a BH remnant, both intrinsic (orange solid line) and observed (red dashed line), i.e. with a correction for absorption by the kilonova ejecta of the form $\propto (1 - e^{-(t/t_{thin})^2})$, where $t_{thin} \approx 1000$ days (Eq.6). And, (2) magnetar spin-down luminosity (Eq. 10, dotted blue line) for $B \sim 10^9$ G to match the level of the observed X-ray emission.

In analogy with X-ray binaries in the “ultra luminous” state (Gladstone et al. 2009) the spectra of stellar mass BHs accreting close to the Eddington luminosity (e.g., Ultraluminous X-ray sources, ULXs, Walton et al. 2018) due to powerful disk outflows that generate a narrow accretion funnel (King 2009). We have normalized $f_b$ to a lower limit based on the observer’s viewing angle Mooley et al. (2018a); Hotokezaka et al. (2019); Ghirlanda et al. (2019) $\theta_{obs} \approx 0.4$ with respective to the original binary axis ($\approx$ accretion disk angular momentum axis): $f_{b,\text{min}} \approx \theta_{obs}^2/2 \sim 0.1$.

In analogy with X-ray binaries in the “ultra luminous” state (Gladstone et al. 2009) the spectra of stellar mass BHs accreting close to the Eddington rate are satisfactorily modeled by a thermal accretion disk plus power-law component with a high-energy exponential break. Ignoring relativistic terms and color corrections, the effective temperature of the disk emission can be estimated as

$$2\pi R_{isco}^2 \sigma T_{eff}^4 = f_b L_X, \quad (4)$$

where $R_{isco} \approx 3GM_*/c^2$ is the innermost radius of the disk for a BH of spin $a \approx 0.6 - 0.8$. This gives

$$kT_{eff} \approx 2\text{ keV} \left( \frac{f_b}{0.1} \right)^{1/4} \times \left( \frac{L_X}{5 \times 10^{38} \text{ erg s}^{-1}} \right)^{1/4} \left( \frac{M_*/2.5M_\odot}{M_{ej}} \right)^{1/2}, \quad (5)$$

i.e. in the range of the CXO sensitivity window for the observed $L_X \approx 5 \times 10^{38} \text{ erg s}^{-1}$ at $t_{now} \sim 10^3$ days, the accretion power on a timescale of $t_{KN} \sim 1$ week after the merger would be higher by a factor $\sim (t_{now}/t_{KN})^{5/3} \approx 4000$, or $\sim 2 \times 10^{42}$ erg s$^{-1}$. The bolometric UV/optical/IR emission (Cowperthwaite et al. 2017; Arcavi 2018; Waxman et al. 2018) from the kilonova of GW 170817 reached $L \approx 10^{41}$ erg s$^{-1}$. The accretion
power would thus exceed the bolometric output of the kilonova on this timescale by a factor $\geq 10$. Even more stringently, extrapolating back to the last HST optical detection of GW 170817 at $\approx 360$ days since merger leads to values $\approx 10^4$ times larger than the observed HST luminosity. At 360 days the optical flux density inferred from HST observations is perfectly consistent with the power-law spectrum that extends from the radio band to the X-rays (Fong et al. 2019) and it is thus dominated by jet-afterglow emission.

However, there are two effects that act to alleviate these constraints. Firstly, at these earlier epochs the fall-back rate is highly super-Eddington. The efficiency with which the fall-back material reaches the central black hole may be drastically reduced at these early times due to the inability of the super-Eddington accretion to radiatively cool (Rossi & Begelman 2009). Furthermore, the radiative efficiency $\eta$ of highly super-Eddington accretion flows may be substantially reduced relative to the near or sub-Eddington accretion rate which characterizes the present epoch. Finally, it is unclear if most of the reprocessed power will emerge in the optical/NIR bands; if lanthanide-series atoms dominate the cooling of the gas in the nebular phase then much of the reprocessed emission may emerge in the mid-IR bands (Hotokezaka et al. 2021). On the other hand, Spitzer observations (Villar et al. 2018; Kasiwai et al. 2019) revealed the 4.5$\mu$m luminosity to be $\approx 10^{38}$ erg s$^{-1}$ on a timescale $\approx 74$ days after the merger, at which time the fall-back accretion rate would be a factor $\approx 100$ higher than at present epoch. Thus we conclude that the reprocessing into the IR band is not a viable option, and would have to rely instead on the reduced accretion efficiency of the fall-back material onto the BH.

We end by commenting on the expected broadband spectrum. If the GW 170817 remnant is accreting at or close to the Eddington limit, it is valuable to contrast its observational properties with those of the ultra-luminous X-ray sources (ULXs), which accrete at or above the Eddington limit for compact objects at $\sim 1 M_\odot$.

Radio observations of ULX sources place upper limits on the radio power of $L_R \lesssim 10^{24}$ erg s$^{-1}$ Hz$^{-1}$ (Körding et al. 2005), corresponding to a flux density limit of $\lesssim 1 \mu$Jy at the distance of GW 170817, which is below the level of our latest radio upper limit of $\approx 5 \mu$Jy (3$\times$RMS, §3.1) and comparable to the local image RMS in our deep VLA observations at 3 GHz. The lack of a radio counterpart of GW 170817 is consistent with observations of XRBs in the “soft” state, which can accrete at a significant fraction of the Eddington rate and have no associated persistent radio emission (Fender et al. 2004). Similarly, if GW 170817 is accreting in a “hard” state (associated with an X-ray spectrum peaking at higher energies compared to the soft state), where the X-ray and radio emission are strongly coupled (Corbel et al. 2003), we would only expect a radio flux density of $\sim 10^{22}$ erg s$^{-1}$ Hz$^{-1}$ based on our measured CXO luminosity and the radio X-ray correlation derived from an ensemble of 24 X-ray binaries in the hard state (Gallo et al. 2014). Typically, X-ray binaries are only in the hard state while in quiescence (accreting at some small fraction of the Eddington rate) or while in outburst where they typically make the hard to soft state transition (Dunn et al. 2010) at around $\sim 0.01 L_{Edd}$ to $\sim 0.1 L_{Edd}$. However, high X-ray luminosity hard states have been observed in the XRB GRS 1915+105 (Rushton et al. 2010; Motta et al. 2021), but the associated radio emission would still be well below our detection threshold. We conclude by emphasizing that a solid expectation from this scenario is that of a different radio-to-X-ray spectrum than the jet afterglow, with less luminous radio emission than expected based on the jet-afterglow spectral slope. This is consistent with our observational findings (§5). Differently from the kilonova afterglow (§7, Figure 9), in the BH fall-back accretion scenario the X-ray luminosity is expected to continuously decrease with time (Figure 11).

To conclude, an accretion-powered origin of the emerging component of X-ray emission is a potentially viable explanation and would naturally account for the broadband spectrum if the efficiency of the super-Eddington fall-back matter reaching the black hole is suppressed sufficiently to prevent the accretion luminosity from violating the observed kilonova luminosity at earlier times. This scenario is further supported by $\alpha$-viscosity hydrodynamical simulations presented in Metzger & Fernandez (2021).

8.2. Spinning-down magnetar scenario

Alternatively, the additional X-ray component could be powered by spin-down energy from a long-lived magnetar remnant (Piro et al. 2019; Troja et al. 2020, see however Radice et al. 2018a). While there are theoretical arguments against the long-lived magnetar remnant scenario (Margalit & Metzger 2017), we consider this scenario here for completeness.

The massive NS remnant created by a BNS merger will in general have more than sufficient angular momentum to be rotating near break-up (Radice et al. 2018a). A NS of mass $M_{\text{NS}}$ rotating near its mass-shedding limit possesses a rotational energy

$$E_{\text{rot}} = \frac{1}{2} I \Omega^2 \approx 1 \times 10^{53} \left(\frac{I}{I_{\text{LS}}}\right) \times \left(\frac{M_{\text{NS}}}{2.5M_\odot}\right)^{3/2} \left(\frac{P}{0.7\text{ms}}\right)^{-2} \text{erg}, \quad (7)$$

where $P = 2\pi/\Omega$ is the rotational period and $I$ is the NS moment of inertia, which we have normalized to an approximate value for a relatively wide class of nuclear equations of state $I_{\text{LS}} \approx 1.3 \times 10^{45}(M_{\text{NS}}/1.4M_\odot)^{3/2}$ g cm$^2$ (Lattimer & Schutz 2005).

The spin-down luminosity $L_{\text{sd}}$ of an aligned dipole rotator of surface field strength $B$ with $I = I_{\text{LS}}$ is (Philippov et al.

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5 We note that a similar scenario has been proposed by Ishizaki et al. (2021), which was released a few days after a first version of this paper appeared on the arXiv.

6 We note that the thermal X-ray luminosity of a cooling NS at this epoch is expected to be $\ll L_{X,\text{obs}} \approx 5 \times 10^{38}$ erg s$^{-1}$ (see Figure 9 in Beznogov et al. 2020).
\[ L_{\text{sd}} = 7 \times 10^{50} \text{ erg s}^{-1} \left( \frac{B}{10^{15} \text{ G}} \right)^2 \times \left( \frac{P_0}{0.7 \text{ ms}} \right)^{-4} \left( 1 + \frac{t}{t_{\text{sd}}} \right)^{-2} \]  

where we have taken \( R_{\text{ns}} = 12 \text{ km} \) as the NS radius, and

\[ t_{\text{sd}} = \left. \frac{E_{\text{sd}}}{L_{\text{sd}}} \right|_{t=0} \approx 150 \text{ s} \left( \frac{I}{I_{\text{LS}}} \right) \left( \frac{B}{10^{15} \text{ G}} \right)^{-2} \left( \frac{P_0}{0.7 \text{ ms}} \right)^2 \]  

is the characteristic spin-down time over which an order unity fraction of the rotational energy is removed, where \( P_0 \) is the initial spin-period and we have assumed a remnant mass of \( M = 2.3 M_\odot \).

The natural spin-down timescale, \( t_{\text{sd}} \), of \( \sim 150 \) seconds (Equation 9), is \( \sim 6 \) orders of magnitude shorter than the observed \( \sim 1000 \) day timescale for the emergence of excess X-ray emission. Accommodating \( t_{\text{sd}} \) to much-increased \( \sim 1000 \) day timescale implies an a-priori unlikely reduction in the magnetic field, an increase of the initial spin period, or both. From Eq. 8:

\[ L_{\text{sd}} \approx 7 \times 10^{50} \text{ erg s}^{-1} \left( \frac{I}{I_{\text{LS}}} \right) \left( \frac{B}{10^{15} \text{ G}} \right)^2 \left( \frac{P_0}{0.7 \text{ ms}} \right)^{-4} \]  

Matching the observed excess X-ray luminosity \( L_X \sim 5 \times 10^{38} \text{ erg s}^{-1} \) would require an extremely weak magnetic field, \( B \sim 10^9 \text{ G} \). While this value is in the range of B inferred for recycled pulsars, this magnetic field is much smaller than the field strength \( \gtrsim 10^{16} \text{ G} \) expected to be amplified inside the remnant during the merger processes (Kishizuka et al. 2015). The calculations above do not include the effects related to gravitational-wave losses that have been proposed in the context of the long-lived NS remnant scenario to dominate the magnetar spin-down at early times to avoid violating the inferred kilonova energy. However, it would still require fine-tuning to match \( L_{\text{sd}} \) to the observed \( L_X \) for a more physical value of \( B \). Furthermore, unlike the BH case (Eq. 5), there is no reason \textit{a priori} to expect the magnetar emission to be largely confined to the X-ray range.

9. SUMMARY AND CONCLUSIONS

We presented the results from our coordinated \textit{CXO}, VLA and MeerKAT campaign of \( GW 170817 \) at \( \delta t = 900 - 1273 \) days (March 2020 to February 2021). Our observations are public and have been partially presented by Troja et al. (2020) (for data at \( \delta t < 950 \) days), Balasubramanian et al. (2021), and Troja et al. (2021). Our X-ray observations at \( \delta t = 940 \) and 1234 days provide the first evidence for a statistically significant deviation from the off-axis jet model and the emergence of a new X-ray component of emission.\footnote{We note that the \( \delta t = 940 \) day dataset would not on its own establish a statistically-significant excess over prior extrapolations.} Our detailed observational findings can be summarized as follows:

- We found evidence for bright X-ray emission from \( GW 170817 \) with a statistical significance of \( 7.2 \sigma \) (§2.1) at \( \delta t \approx 1234 \) days with luminosity of \( \sim 5 \times 10^{38} \text{ erg s}^{-1} \). This emission is a factor \( \approx 4 \) larger than the extrapolation of the structured-jet model to the present epoch (Figure 2). We employed two independent approaches to estimate the statistical significance of the X-ray excess. For both approaches the statistical tests are performed in the count-rate phase space to minimize the role of any effect related to the flux calibration and self-consistently account for the Poisson nature of the process. The first approach utilizes multi-wavelength jet afterglow light-curves generated with JetFit, while the second approach is jet-model agnostic and adopts an achromatic simple power-law flux decay. Based on these two independent tests we conclude that the \textit{CXO} observations at \( \delta t > 900 \) days support the evidence of an excess of X-ray emission compared to the predictions from the earlier broadband evolution with statistical significance in the range \( 3.1 \sigma - 3.9 \sigma \).

- In contrast to the X-rays, we find no evidence for significant radio emission at the location of \( GW 170817 \) (Figure 2, lower panel, and Figure 1), and we place \( 3 \sigma \) flux density upper limits of 39, 5.1, and 5.1 \( \mu \text{Jy} \) at mean frequencies of 0.8, 3 and 15 GHz, respectively, with MeerKAT and the VLA (3×RMS, §3.1 and §3.2).

- While there is no evidence for X-ray spectral evolution using the X-ray data alone, the lack of detectable radio emission at the time of the X-ray excess suggests hardening of the non-thermal emission from \( GW 170817 \) (Figure 5) compared to jet afterglow with a statistical confidence \( \geq 99\%-99.2\% \) (Figure 6). Therefore, these results suggest the evolution of the radio-to-X-ray broadband spectrum towards lower values of \( p \) (where the spectrum is \( F_\nu \propto \nu^{-(p-1)/2} \) and constitute the first indication of spectral evolution of the non-thermal emission from \( GW 170817 \) (Figure 5). The radio flux density recently reported by Balasubramanian et al. (2021) further strengthens these conclusions (Figure 6).

A number of factors could in principle lead to a late-time X-ray light-curve flattening as the observations suggest. We discuss the late-time evolution of the jet in §6 as one of the potential scenarios and conclude that to explain the excess of emission it would require an ad hoc evolution of key physical parameters of the system and is thus disfavored. We pro-
pose two alternative explanations: (i) the emergence the kilonova afterglow; (ii) emission from accretion processes on the compact-object remnant.

The emergence of the kilonova afterglow, which originates from a quasi-spherical shock that is different from the jet afterglow shock, can naturally explain the observed broadband spectral evolution of the radiation, as the value of $p$ may be different in the two shocks. In this context the lower value of $p$ suggested by our observations is consistent with the expectations from the theory of Fermi acceleration in the test particle limit (Bell 1978; Blanford & Ostriker 1978; Blanford & Eichler 1987) for mildly relativistic shocks, such as that produced by the kilonova. From our exploration of the kilonova afterglow emission with analytical kinetic energy profiles ($E_{KN}(\Gamma \beta) \propto (\Gamma \beta)^{-\alpha}$, §7.1) and physically-motivated $E_{KN}(\Gamma \beta)$ (§7.2, Figure 10) we find that ejecta profiles with $\alpha = 4 - 6$ can reasonably account for observations at $\delta t > 900$ day (Figure 2). However, as discussed in §7.1, the parameter space is currently poorly constrained (Figure 7). Similarly, we find that a variety of NS EoS and binary mass ratios can accommodate our observations (also see Nedora et al. 2021a). However, a common ingredient of successful models is binaries that do not undergo prompt black hole (BH) collapse. Finally, the presence of a very fast kilonova ejecta component (Figure 10) has important implications on still-open questions pertaining to the existence of a free-neutron component of the ejecta possibly powering a short-lived luminous UV/optical transient, and the origin of subluminous gamma-rays produced in GRB 170817A from the breakout of the cocoon shock from the merger ejecta.

Radiation powered by an energy release associated with the compact-object remnant in the form of accretion on a BH remnant offers an alternative explanation to the presence of an X-ray excess that is not accompanied by bright radio emission ($\S$8.1). The detected X-ray luminosity $L_\text{x} \sim 5 \times 10^{38} \text{erg s}^{-1}$ is $\approx L_{\text{Edd}}$ for a compact-object with mass of a few $M_\odot$. A long-lived NS cannot be entirely ruled out, but we conclude that it is an unlikely scenario based on the exceedingly low magnetic field $B \approx 10^8 \text{G}$ necessary to match the observed X-ray luminosity ($\S$8.2). In analogy to stellar-mass compact-objects accreting close to or above the Eddington rate, i.e. X-ray binaries (XRBs) in the “soft” state and ultra-luminous X-ray (ULXs) sources significant suppression of the radio emission can be expected. Unlike the kilonova afterglow, where the radio emission is expected to brighten with time (Figure 2), this accretion model predicts a constant or declining X-ray emission without accompanying bright radio emission.

Observations of GW170817 are mapping an uncharted territory of the BNS merger phenomenology and have far-reaching theoretical implications. Measuring the time of peak of the kilonova afterglow, which probed the ejecta dynamics independent of shock microphysics, would offer a unique opportunity to do calorimetry of the kilonova’s fastest ejecta. Alternatively, the detection of a constant (or declining) source of X-ray emission in the next thousands of days that is not accompanied by bright radio emission will unveil how accretion processes work on a compact-object remnant of a BNS merger a few years after its birth.

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We provide two flux calibrations for the latest two epochs at δt ≈ 939 and 1234 days for which the photon statistics is too limited to constrain the photon index: first we assume a photon index that is the best fitting value from the joint spectral fitting of all CXO observations Γ = 1.603 (see §2.2). Second, we provide a flux calibration that assumes a spectral model consistent with a jet afterglow origin of the detected X-rays. From the posterior distribution of the p parameter of models presented in §4, we infer Γ = 1.565 ± 0.025.

![Table 1](https://example.com/table1.png)

| δt  | Significance | Exposure | Net count-rate | Γ          | Unabsorbed Flux | Luminosity | PI     |
|-----|--------------|----------|----------------|------------|----------------|------------|--------|
| (days) | (σ) | (ks) | (10⁻⁴ ct/s) (0.5-8 keV) | (10⁻¹⁵ erg cm⁻² s⁻¹) (0.3-10 keV) | (10³⁸ erg s⁻¹) (0.3-10 keV) |         |
| 2.33 | 0.3   | 24.60 | < 1.2 | 1.4 | < 1.9 | < 3.75 | Fong |
| 9.19 | > 8 | 49.41 | 2.36 ± 0.70 | 0.78³⁺⁰.⁶⁷⁻⁻⁰.⁵⁶ | 6.80³⁺².⁸²⁻⁻².⁹² | 13.⁵⁺⁵.⁵⁹⁻⁻⁵.⁷⁹ | Troja |
| 15.39 | > 8 | 96.1 | 2.95 ± 0.56 | 2.⁰⁵⁺¹.⁴⁹⁻⁻¹.⁳³ | 5.³³⁺¹.⁴²⁻⁻⁰.⁹⁹ | 10.⁶⁺².⁸¹⁻⁻¹.⁹⁷ | Haggard, Troja |
| 108.39 | > 8 | 98.83 | 13.⁵ ± 1.17 | 1.⁵⁸⁺⁰.⁶⁰⁻⁻⁰.₁⁶ | 25.⁶⁺².⁴⁹⁻⁻².³⁴ | 50.⁸⁺⁴.⁹³⁻⁻⁴.⁴⁵ | Wilkes |
| 157.76 | > 8 | 104.85 | 13.⁷ ± 1.14 | 1.⁶⁴⁺¹.⁵⁵⁻⁻⁰.¹⁸ | 26.⁷⁺².⁹⁰⁻⁻².³³ | 52.⁸⁺⁵.⁷⁴⁻⁻⁴.⁶³ | Wilkes |
| 259.67 | > 8 | 96.78 | 6.⁸⁵ ± 0.⁸⁵ | 1.⁴⁷⁺¹.²³⁻⁻¹.⁲² | 13.⁹⁺².¹³⁻⁻².⁰¹ | 27.⁶⁺⁴.²²⁻⁻³.⁹⁸ | Wilkes |
| 358.61 | > 8 | 67.16 | 3.⁹⁴ ± 0.⁷⁷ | 2.⁰²⁺¹.⁴⁴⁻⁻⁰.⁳⁴ | 7.⁶⁷⁺¹.⁷⁶⁻⁻¹.⁴⁶ | 15.⁲⁺³.⁵⁰⁻⁻².⁸⁹ | Troja |
| 581.82 | > 8 | 98.76 | 1.⁴⁴ ± 0.⁳⁹ | 1.¹⁹⁺¹.⁸⁹⁻⁻⁰.⁶⁰ | 3.⁸⁸⁺¹.⁹⁷⁻⁻¹.⁴⁰ | 7.⁶⁸⁺³.⁹⁰⁻⁻².⁷⁷ | Margutti |
| 741.48 | 6.⁵ | 98.86 | 1.⁰³ ± 0.³⁴ | 0.⁹²⁺¹.⁹¹⁻⁻⁰.⁷⁷ | 3.³³⁺¹.⁷⁵⁻⁻¹.⁴² | 6.⁵⁺³.⁴⁶⁻⁻².⁸¹ | Troja |
| 939.31 | 5.⁴ | 96.60 | 0.⁷⁵ ± 0.²⁹ | 1.⁶⁰³ | 1.⁸³⁺⁰.⁷⁹⁻⁻⁰.⁹⁴ | 3.⁵⁹⁺¹.⁵⁷⁻⁻¹.⁸⁶ | Margutti |
| 1234.11 | 7.⁲ | 189.⁰⁶ | 0.⁷⁷ ± 0.²¹ | 1.⁶⁰³ | 2.³³⁺⁰.⁵⁷⁻⁻⁰.⁸¹ | 4.⁵⁺¹.¹³⁻⁻¹.⁶¹ | Margutti |

1 Exposure-time weighted average time since merger of all the observations within an epoch. The obsIDs within each epoch are as follows: 9 days: 19294; 15 days: 18988, 20728; 108 days: 20860, 28061; 158 days: 20936, 20937, 20938, 20939, and 20945; 260d: 21080, and 21090; 359 days: 21371; 582 days: 21322, 22157, and 22158; 742 days: 21372, 22736, and 22737; 939 days: 21323, 23183, 23184, and 23185; and 1234 days: 22677, 24887, 24888, 24889.2, 3870, 24923, and 24924.

2 Gaussian equivalent.

3 Inferred from mcnspec and energy filtering in channels 500-8000.

4 Spectral photon index, where $F_\nu \propto \nu^{-\beta}$ and $\Gamma = \beta + 1$.

5 Calculated using a distance of 40.7 Mpc (Cantiello et al. 2018).

6 From Margutti et al. (2018).
Table 2. Radio Observations Log. Time on source for the VLA observations was calculated using the CASA analysis utilities task `timeOnSource`.

| Start Date   | δt  | Observatory | Program/Project | On Source | Mean Frequency | Frequency Range |
|--------------|-----|-------------|-----------------|-----------|----------------|-----------------|
| 15th Dec. 2020 | 1216.08 | VLA | SL0449 | 204.23 | 3 | 2-4 |
| 27th Dec. 2020 | 1228.02 | VLA | SL0449 | 204.23 | 3 | 2-4 |
| 2nd Feb. 2021 | 1264.95 | VLA | SM0329 | 204.27 | 3 | 2-4 |
| 10th Feb. 2021 | 1272.88 | VLA | SM0329 | 164.40 | 15 | 12-18 |
| 3rd Jan. 2021 | 1234.66 | MeerKAT | DDT-20201218-JB-01 | 434.40 | 0.816 | 0.544-1.088 |

Table 3. Chance probability of measuring a number of X-ray photon counts at least as extreme as the one observed at $t_1$, $t_2$ and combined, as a result of a stochastic fluctuation of the source and background. See §4 for details.

| $t_{start}$ (days) | $P_1$ | $P_2$ | $P_1 \times P_2$ | $P_{combined}$ |
|---------------------|-------|-------|-------------------|-----------------|
| 157.                 | 6.0x10^{-2} | 2.6x10^{-4} | 1.7x10^{-5} | 9.5x10^{-5} |
| 163.                 | 1.1x10^{-1} | 9.7x10^{-4} | 1.2x10^{-4} | 6.7x10^{-4} |
| 172.                 | 1.2x10^{-1} | 1.2x10^{-3} | 1.8x10^{-4} | 9.5x10^{-4} |
| 196.                 | 1.4x10^{-1} | 1.5x10^{-3} | 2.5x10^{-4} | 1.4x10^{-4} |
| 209.                 | 1.4x10^{-1} | 1.5x10^{-3} | 2.5x10^{-4} | 1.3x10^{-4} |
| 215.                 | 1.3x10^{-1} | 1.5x10^{-3} | 2.4x10^{-4} | 1.2x10^{-4} |
| 230.                 | 1.4x10^{-1} | 1.5x10^{-3} | 2.4x10^{-4} | 1.3x10^{-4} |
| $\gamma_B$ | $P_1$ | $P_2$ | $P_1 \times P_2$ | $P_{combined}$ |
|---------------------|-------|-------|-------------------|-----------------|
| 7                   | 1.5x10^{-1} | 2.8x10^{-3} | 4.7x10^{-4} | 2.1x10^{-3} |
| 10                  | 1.2x10^{-1} | 2.7x10^{-3} | 3.4x10^{-4} | 1.4x10^{-3} |
| 12                  | 7.2x10^{-2} | 7.4x10^{-4} | 5.6x10^{-5} | 2.6x10^{-4} |
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REFERENCES

Abbott, B. P., Abbott, R., Abbott, T. D., et al. 2017a, ApJL, 848, L12, doi: 10.3847/2041-8213/aa91c9
—. 2017b, PhRvL, 119, 161101, doi: 10.1103/PhysRevLett.119.161101
—. 2019, Physical Review X, 9, 011001, doi: 10.1103/PhysRevX.9.011001
Achterberg, A., Gallant, Y. A., Kirk, J. G., & Guthmann, A. W. 2001, MNRAS, 328, 393, doi: 10.1046/j.1365-8711.2001.04851.x
Alexander, K. D., Margutti, R., Blanchard, P. K., et al. 2018, ApJL, 863, L18, doi: 10.3847/2041-8213/aad637
Arcavi, I. 2018, ApJL, 855, L23, doi: 10.3847/2041-8213/aab267
Balasubramanian, A., Corsi, A., Mooley, K. P., et al. 2021, arXiv e-prints, arXiv:2103.04821. https://arxiv.org/abs/2103.04821
Beznogov, M. V., Page, D., & Ramirez-Ruiz, E. 2020, ApJ, 888, 97, doi: 10.3847/1538-4357/ab5fd6
Bell, A. R. 1978, MNRAS, 182, 147, doi: 10.1093/mnras/182.2.147
Berti, S., Breschi, M., Douchin, F., & Haensel, P. 2001, A&A, 380, 153, doi: 10.1051/0004-6361:20001402
Blanchard, P., Berger, E., Fong, W., et al. 2017, The Astrophysical Journal, 848, L21, doi: 10.3847/2041-8213/aa905d
Blanchard, P., Berger, E., Fong, W., et al. 2017, The Astrophysical Journal Letters, 848, L22
Blandford, R., & Eichler, D. 1987, PhR, 154, 1, doi: 10.1103/epja/10050-019-00018-6
Bromberg, O., Tchekhovskoy, A., Gottlieb, O., Nakar, E., & Piran, T. 2018, MNRAS, 475, 2971, doi: 10.1093/mnras/stx3316
Bulik, T., Covino, S., Kutyk, K., et al. 2019, Nature Astronomy, 3, 99, doi: 10.1038/s41550-018-0593-y
Cantiello, M., Jensen, J. B., Blakeslee, J. P., et al. 2018, ApJL, 854, L31, doi: 10.3847/2041-8213/aaad64
Ciolfi, R. 2020, MNRAS, 495, L66, doi: 10.1093/mnrasl/slaa062
Corbel, S., Nowak, M. A., Fender, R. P., Tzioumis, A. K., & Markoff, S. 2003, A&A, 400, 1007, doi: 10.1051/0004-6361:20030090
Cowperthwaite, P. S., Berger, E., Villar, V. A., et al. 2017, ApJ, 848, L17, doi: 10.3847/2041-8213/aa8fc7
Crumley, P., Caprioli, D., Markoff, S., & Spitkovsky, A. 2019, MNRAS, 485, 5105, doi: 10.1093/mnras/stz232
Dobie, D., Kaplan, D. L., Murphy, T., et al. 2018, ApJ, 858, L15, doi: 10.3847/2041-8213/aa105
Douchin, F., & Haensel, P. 2001, A&A, 380, 151, doi: 10.1051/0004-6361:20011402
Drouet, M. R., Piro, A. L., Shappee, B. J., et al. 2017, Science, 358, 1570, doi: 10.1126/science.aaq0049
Duffell, P. C., & MacFadyen, A. I. 2013, ApJL, 776, L9, doi: 10.1088/2041-8205/776/1/L9
Dunn, R. J. H., Fender, R. P., Körding, E. G., Belloni, T., & Cabanac, C. 2010, MNRAS, 403, 61, doi: 10.1111/j.1365-2966.2010.16114.x
Endrizzi, R., Perego, A., Fabrizio, F. M., et al. 2020, European Physical Journal A, 56, 15, doi: 10.1140/epja/s10050-019-00018-6
Evans, P. A., Cenko, S. B., Kennea, J. A., et al. 2017, Science, 358, 1565, doi: 10.1126/science.aap9580
Fender, R. P., Belloni, T. M., & Gallo, E. 2004, MNRAS, 355, 1105, doi: 10.1111/j.1365-2966.2004.08384.x
Fernández, R., & Metzger, B. D. 2013, MNRAS, 435, 502, doi: 10.1093/mnras/stt9312
Fong, W., Blanchard, P. K., Alexander, K. D., et al. 2019, ApJL, 883, L1, doi: 10.3847/2041-8213/ab3d9e
Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, PASP, 125, 306, doi: 10.1086/670067
Frais, D. A., Waxman, E., & Kulkarni, S. R. 2000, ApJ, 537, 191, doi: 10.1086/309024
Fruscione, A., McDowell, J. C., Allen, G. E., et al. 2006, in Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, Vol. 6270, Society of Photo-Optical Instrumentation Engineers (SPIE) Conference Series, 62701V, doi: 10.1117/12.671760
Gallo, E., Miller-Jones, J. C. A., Russell, D. M., et al. 2014, MNRAS, 445, 290, doi: 10.1093/mnras/stt1312
Ghirlanda, G., Salafia, O. S., Paragi, Z., et al. 2019, Science, 366, 968, doi: 10.1126/science.aau8815
Gill, R., Nathanael, A., & Rezzolla, L. 2019, ApJ, 876, 139, doi: 10.3847/1538-4357/ab16da
Gladstone, J. C., Roberts, T. P., & Done, C. 2009, MNRAS, 397, 1836, doi: 10.1111/j.1365-2966.2009.15123.x
Goldstein, A., Veres, P., Burns, E., et al. 2017, ApJL, 848, L14, doi: 10.3847/2041-8213/aa8f41
[Reference Text]
Tasse, C., Hugo, B., Mirmont, M., et al. 2018, A&A, 611, A87, doi: 10.1051/0004-6361/201731474
Troja, E., Piro, L., Ryan, G., et al. 2018, MNRAS, 478, L18, doi: 10.1093/mnrasl/sly061
Troja, E., van Eerten, H., Ryan, G., et al. 2019, MNRAS, 2169, doi: 10.1093/mnras/stz2248
Troja, E., van Eerten, H., Zhang, B., et al. 2020, MNRAS, 498, 5643, doi: 10.1093/mnras/staa2626
Troja, E., O’Connor, B., Ryan, G., et al. 2021, arXiv e-prints, arXiv:2104.13378. https://arxiv.org/abs/2104.13378
Villar, V., Guillochon, J., Berger, E., et al. 2017, ApJL, 851, L21
Villar, V. A., Cowperthwaite, P. S., Berger, E., et al. 2018, ApJL, 862, L11, doi: 10.3847/2041-8213/aad281
Walton, D. J., Bachetti, M., Fürst, F., et al. 2018, ApJ, 857, L3, doi: 10.3847/2041-8213/aabadc
Waxman, E., Ofek, E. O., Kushnir, D., & Gal-Yam, A. 2018, MNRAS, 481, 3423, doi: 10.1093/mnras/sty2441
Wu, Y., & MacFadyen, A. 2018, ApJ, 869, 55, doi: 10.3847/1538-4357/aae9de
—. 2019, ApJL, 880, L23, doi: 10.3847/2041-8213/ab2fd4
Figure 12. Comparison of 1 keV flux densities derived in this work (purple circles, derived from the fluxes reported in Table 1), where we do not assume a photon index based on the jet afterglow modeling, with those calculated by Troja et al. (2021) (orange circles) where also the photon index is free for all epochs, as noted in their Table 1. We note that all the detections are consistent within $\lesssim 0.9\sigma$ uncertainties at all epochs. The colored bands are the 68%, 97.5%, and 99.8% confidence interval of the fits obtained from fitting our data including the latest epochs at $\delta t > 900$ days (purple bands, same as in Figure 4) and from fitting all the data from Troja et al. (2021) (in orange) using JetFit, with $\gamma_B = 12$, $n = 0.01 \text{ cm}^{-3}$, and $\epsilon_e = 0.1$ fixed. Even though these fits were obtained for all the flux densities derived using their respective spectral indices, for plotting purposes only, we have shown our $\delta t > 900$ days flux densities (in purple) that were obtained using a fixed $\Gamma$. The best-fits derived in this work using JetFit with $\gamma_B = 12$ and $\gamma_B = 10$ fixed as discussed in §4 are represented by solid and dashed purple lines, respectively. The best-fits obtained in Troja et al. 2021 are plotted in black lines.

APPENDIX

A. X-RAY FLUX CALIBRATION

In this Appendix we provide additional details on the comparison between the flux calibration of the X-ray data from this work and the analysis of our data set by Troja et al. (2021). Our X-ray data analysis and the limitations of the data treatment by Troja et al. (2021) are described in §2.2. Figure 12 shows that the two flux calibrations lead to X-ray fluxes that are within $0.9\sigma$. There is thus no statistical tension between the two flux calibrations. We further show the best fitting jet-afterglow model that is used by Troja et al. (2021) to compute the significance of the X-ray excess (black solid line, $\theta_{\text{obs}} = 31^\circ$, $\theta_{\text{jet}} = 5^\circ$), as well as the best-fitting model of the entire afterglow light-curve dataset (i.e. including the last two X-ray epochs) by Troja et al. (2021), which has $\theta_{\text{obs}} = 38^\circ$, $\theta_{\text{jet}} = 6^\circ$. This model is in tension with the inferences from the VLBI observations by Mooley et al. (2018a); Ghirlanda et al. (2019). We present with a dashed black line the model by Ryan et al. (2020) (also presented by Troja et al. 2021, their Figure 5) that is consistent with the VLBI measurements, and that would lead to the inference of a larger discrepancy between the late-time X-ray observations and the model expectations.

As a proof of concept we have fitted the data at $\delta t < 1300$ days with JetFit using $\gamma_B = 12$. First, we included the X-ray fluxes from our data reduction where we leave the photon index as a free parameter for all epochs. Even though these fits were obtained for all the flux densities derived using their respective spectral indices, for plotting purposes only, we have shown our $\delta t > 900$ days flux densities (purple points in Figure 12) that were obtained using a fixed $\Gamma$. Second, we have repeated the same exercise by including the X-ray fluxes by Troja et al. (2021). Figure 12 shows complete overlap of the 68% confidence regions of the two best-fitting models at all times.
In this paper, we have calculated the significance of a deviation of the observed X-rays using two different approaches - a jet-model dependent analysis, and a more universal, jet-model independent analysis. Both analyses independently result in an excess of X-ray emission with $\geq 3.1\sigma$ (Gaussian equivalent) confidence level. In Figure 13, we show the best-fitting universal post jet-break model. As mentioned in §4, the fitting included the observations taken between $t_{\text{start}} < t < 900$ days. As seen from Figure 13, and the residual plot in the top panel of Figure 4, the fits start gradually diverging (although not to any significant level) from the data at $t > 300$ days. This further strengthens our argument on the emergence of a new component of emission as it is likely to gradually manifest with time, as opposed to an abrupt appearance at some point in time, as the jet afterglow fades away.

**Figure 13.** One- and two-dimensional projections of the posterior distributions of the model’s free parameters. Vertical dashed lines mark the 16th, 50th, and 84th percentiles of the marginalized distributions (i.e. the median and 1-$\sigma$ range). The contours are drawn at 68%, 95%, and 99% credible levels.

**B. JETFIT CORNER PLOT**

In this paper, we have calculated the significance of a deviation of the observed X-rays using two different approaches - a jet-model dependent analysis, and a more universal, jet-model independent analysis. Both analyses independently result in an excess of X-ray emission with $\geq 3.1\sigma$ (Gaussian equivalent) confidence level. In Figure 13, we show the best-fitting universal post jet-break model. As mentioned in §4, the fitting included the observations taken between $t_{\text{start}} < t < 900$ days. As seen from Figure 13, and the residual plot in the top panel of Figure 4, the fits start gradually diverging (although not to any significant level) from the data at $t > 300$ days. This further strengthens our argument on the emergence of a new component of emission as it is likely to gradually manifest with time, as opposed to an abrupt appearance at some point in time, as the jet afterglow fades away.