Minimal $Z'$ models for flavor anomalies

Richard H. Benavides,1,* Luis Muñoz,1,† William A. Ponce,2,‡ Oscar Rodríguez,1,2,§ and Eduardo Rojas3,¶

1Facultad de Ciencias Exactas y Aplicadas, Instituto Tecnológico Metropolitano, Calle 73 No 76 A - 354, Vía el Volador, Medellín, Colombia
2Instituto de Física, Universidad de Antioquia, Calle 70 No. 52-21, Apartado Aéreo 1226, Medellín, Colombia
3Departamento de Física, Universidad de Nariño, A.A. 1175, San Juan de Pasto, Colombia

By allowing gauge anomaly cancellation between fermions in different families we find a non-universal solution for a $Z'$ family of models with the same content of fermions of the standard model plus three right-handed neutrinos. We also impose constraints from the Yukawa interaction terms in such a way that at the end we obtain a solution with six free parameters. Our solution contains as particular cases well-known models in the literature. As an application, we report a model that evades LHC constraints, flavor changing neutral currents and low energy constraints. Simultaneously, the model is able to explain the flavor anomalies in the Wilson coefficients $C_9(\mu)$ and $C_{10}(\mu)$ without modifying the corresponding Wilson coefficients for the first family. In our approach, this procedure is always possible for $Z'$ masses smaller than $\sim 2.5$ TeV.

PACS numbers: 12.38.-t 11.10.St 11.15.Tk, 14.40.Pq 13.20.Gd 14.40.Df

I. INTRODUCTION

In recent years, experimental anomalies in the LHCb and in low-energy experiments [1–4] have generated some theoretical speculation about the possibility that these results constitute a manifestation of physics beyond the standard model (SM). A number of anomalies in semileptonic $B$ decays have been reported by the LHCb collaboration and other experiments [2, 5–10], finding various deviations from their predicted values in the SM. Even though the experimental results are not conclusive yet, the global fits improve for models where the new physics contributions to the Wilson coefficient $C_9(\mu)$ decrease it by a quarter of the SM prediction [11]. Because the only lepton in the associated Wilson operator is the muon field, one of the preferred theoretical frameworks to explain these anomalies are the non-universal models [12–20], for which the electroweak (EW) parameters and quantum numbers are family dependent. In general, non-universal models are restricted severely by flavor changing neutral currents (FCNC); however, as it is well-known [21], we can get rid of these problems by guaranteeing that the gauge couplings of the new physics to the left-handed down-type quarks become identical (We do not know anything about the mixing of the right-handed quarks so that we can assume a diagonal matrix. That result quite useful to avoid further constraints on the $Z'$ charges). That is particularly important for the first and second generation.

The best-known non-universal EW extensions of the SM correspond to the so-called 331 models; however, simpler solutions can be built by restricting the additional EW sector to an abelian $U(1)$ gauge symmetry with the same fermion content of the SM plus right-handed neutrinos. As we will show, these minimal solutions are able to explain these anomalies without increasing the number of new fields and parameters. These EW extensions are known as minimal models [22–33], and constitute the simplest EW extension of the SM. The best-known example is the left-right symmetric (LRS) model, which has universal EW charges for the three families and its content of fermions excess the SM one by a right-handed neutrino in every family. Earlier in the nineties, several works pointed out the non-fundamental character of the universality of the EW charges [34–45]. This was motivated by EW models based on string theory which, in most of the cases, result to be non-universal [26]. A general solution to the gauge anomalies involves a cubic Diophantine equation [46]; however, it is possible to find solutions with continuous parameters, which turn out quite useful to build benchmark models.

A lot of phenomenology has been based on the minimal models [13–16, 24, 27, 47–60], in spite of it, most of these analysis make use of some few well-known EW charge assignments leaving aside other possible solutions to the gauge anomaly equations with the same content of fermions. A first step to know the full set of solutions was given in

*Electronic address: richardbenavides@itm.edu.co
†Electronic address: luismunoz@itm.edu.co
‡Electronic address: william.ponce@udea.edu.co
§Electronic address: oscara.rodriguez@udea.edu.co
¶Electronic address: eduro4000@gmail.com
our previous work [62], where we assume two identical families and the non-universality show up only in the third generation. In the present manuscript, we allow non-universal charges for leptons and quarks in the three families, which result quite convenient in the study of the LHCb anomalies. Under some reasonable assumptions, many of these models are able to evade the FCNC constraints.

The paper is organized as follows: in Section II we derive the general expressions for the chiral charges of the models. In Section IV we derive the 95% C.L. allowed limits on the model parameters by the most recent LHC data and the corresponding limits by the low energy EW data. Section V summarizes our conclusions.

II. THE $SU(2)_L \otimes U(1) \otimes U(1)'$ GAUGE SYMMETRY

The aim of the present work is to build the most general parameterization for the minimal EW extension of the SM, limiting ourselves to the SM fermions plus right-handed neutrinos. In order to accomplish our purpose it is necessary to avoid the hypothesis of universality; with this in mind, let us consider the gauge group $SU(2) \otimes U(1) \otimes U(1)'$ as a non-universal anomaly-free extension of the EW sector of the SM.

In what follows $T_{1L}, T_{2L}$ and $T_{3L}$ denote the generators of $SU(2)_L$, while $Y$ and $Q_{Z'}$ denote the generators of $U(1)$ and $U(1)'$, respectively. The covariant derivative for our model is given by [63]

$$D_\mu = \partial_\mu - ig_1 \mathbf{T}_1 \cdot \mathbf{A}_\mu - ig_2 Y B_{Y\mu} - ig_2 Q_{Z'} Z'_\mu,$$

where $g_1, g_Y$ and $g_{Z'}$ are the gauge couplings associated with the $SU(2)_L$, $U(1)$ and $U(1)'$ gauge groups, respectively, and $\mathbf{T}_1$, $B_{Y\mu}$ and $Z'\mu$ denote the corresponding gauge fields.

In order to find the most general solution to gauge anomaly cancellation, all families have different quantum numbers, because of this, at least two Higgs doublets are required in order to give masses to the three families, so:

$$\langle \Phi_i \rangle = (0, v_i/\sqrt{2}), \quad i = 1, 2.$$  \hspace{1cm} (2)

At this stage, it is important to stress that we do not intend to report a model, instead our purpose is to show a general solution to the anomaly cancellation equations. We added two Higgs doublets since it represents the minimal scalar field content in order to have Yukawa couplings for a non-universal $Z'$ gauge boson. In our solution, every set of parameters represents a possibile electroweak model. For every choice of the $Z'$ charges it is possible to choose additional scalars in order to reproduce the mixing angles in the lepton and quark sectors. From general grounds, with the Higgs structure of our model it is possible to generate mass matrices with four texture zeros in the lepton and quark sectors. That is possible since in that our solution two families couple to a single Higgs doublet and just one of the families couples to a different scalar doublet. It is well-known that even mass matrices with five texture zeros are able to generate the mixing matrices for the lepton and quark sectors [61]. Thus in principle it is not forbidden for four texture zero mass matrices to generate the CKM and PMNS mixings. Any case, as we mentioned above, for a particular choice of the $Z'$ charges there is possible to add new scalars if needed.

A. Gauge anomaly cancellation

For the $SU(2)_L \otimes U(1) \otimes U(1)'$ symmetry with the particle content shown in table I, the non-trivial gauge anomaly equations are:

$$[SU(2)]^2 U(1)': 0 = \Sigma q + \frac{1}{3} \Sigma l,$$

$$[SU(3)]^2 U(1)' : 0 = 2 \Sigma q - \Sigma u - \Sigma d,$$

$$[\text{grav}]^2 U(1)' : 0 = 6 \Sigma q - 3(\Sigma u + \Sigma d) + 2 \Sigma l - \Sigma n - \Sigma e,$$

$$[U(1)]^2 U(1)' : 0 = \frac{1}{3} \Sigma q - \frac{8}{3} \Sigma u - \frac{2}{3} \Sigma d + \Sigma l - 2 \Sigma e,$$

$$U(1)[U(1)']^2 : 0 = \Sigma q^2 - 2 \Sigma u^2 + \Sigma d^2 - \Sigma l^2 + \Sigma e^2,$$

$$[U(1)']^3 : 0 = 6 \Sigma q^3 - 3(\Sigma u^3 + \Sigma d^3) + 2 \Sigma l^3 - \Sigma n^3 - \Sigma e^3,$$  \hspace{1cm} (3)
TABLE I: Particle content. The subindex $i = 1, 2, 3$ stand for the family number in the interaction basis. In our solution $\phi_2 = \phi_3$ in such a way that only two Higgs doublets are needed. However, sometimes we keep the notation $\phi_i$, which is quite convenient for notation purposes.

where $\Sigma f = f_1 + f_2 + f_3$. We also take into account the constraints coming from the Yukawa couplings:

$$L_Y \supset \bar{l}_1 L \Phi_1 \nu_1 + \bar{l}_1 L \Phi_1 e_1 + \bar{u}_1 L \Phi_1 u_1 + \bar{u}_1 L \Phi_1 u_1 +$$

$$\bar{e}_2 \Phi_2 \nu_2 + \bar{e}_2 \Phi_2 \nu_2 + \bar{d}_2 \Phi_2 \nu_2 + \bar{d}_2 \Phi_2 \nu_2 +$$

$$\bar{l}_3 \Phi_3 \nu_3 + \bar{l}_3 \Phi_3 \nu_3 + \bar{u}_3 \Phi_3 \nu_3 + \bar{u}_3 \Phi_3 \nu_3 + \text{h.c.}$$

(4)

The corresponding constraints coming from the terms in the above Lagrangian are (where $\phi_2 = \phi_3$):

$$0 = e_i - l_i + \phi_i,$$

$$0 = n_i - l_i - \phi_i,$$

$$0 = d_i - q_i + \phi_i,$$

$$0 = u_i - q_i - \phi_i.$$

(5)

The solution to the gauge anomaly equations (3) and the constraints from the Yukawa interaction terms (5) corresponds to the charges shown in table II (there are six solutions corresponding to the permutations between the indices $ijk$). In general, every one of these solutions depends on six parameters, $(q_i, n_i)$, with $i = 1, 2, 3$, corresponding to the $Z'$ charges for the quark doublet and the right-handed neutrino in every generation, respectively. By removing the constraint $\phi_{ijk}$ there are two additional solutions which will be reported elsewhere since they do not fit well the flavor anomalies.

| Particles | Spin | $SU(3)_C$ | $SU(2)_L$ | $U(1)_Y$ | $U(1)'$ |
|-----------|------|-----------|-----------|----------|---------|
| $l_L$    | 1/2  | 1         | 2         | -1/2     | $l_i$   |
| $e_R$    | 1/2  | 1         | 1         | -1       | $e_i$   |
| $\nu_R$  | 1/2  | 1         | 1         | 0        | $n_i$   |
| $q_L$    | 1/2  | 3         | 2         | 1/6      | $q_i$   |
| $u_R$    | 1/2  | 3         | 1         | 2/3      | $u_i$   |
| $d_R$    | 1/2  | 3         | 1         | -1/3     | $d_i$   |
| $\Phi_i$ | 0    | 1         | 2         | 1/2      | $\phi_i$ |

TABLE II: The $Z'$ couplings for the Higgs doublets $\Phi_i$ and $\Phi_j$ are $\phi_i = n_i + 3q_i$ and $\phi_j = \phi_k = \frac{1}{2}[n_j + n_k + 3(q_j + q_k)]$, respectively. The higgs field $\phi_i$ couples to fermions in the $i$-th family. The integers $ijk$ are a permutation of 123.

By setting $(n_j - n_k)/2 = L_i = -L_k = 1$, $n_k = -1$ and $q_i = q_j = q_k = n_i = 0$, from this solution we can obtain the model $L_j - L_k$ [22] where $L_i$ is 1 for the leptons in the $i$-th family and zero otherwise. From these solutions, the most known model is the $L_\mu - L_\tau$ model, which has been widely used to explain the $g - 2$ anomaly [51].
III. MIXING MATRICES FOR NON-UNIVERSAL Z' MODELS

Since the SM is universal there is no problem with the quantum numbers to generate the mass matrices for the quark and lepton sectors, the same is true for electroweak extensions of the standard model with universal couplings; however, non-universal models require additional scalars to generate the right mixing for the SM fermions.

A. Models with a non-universal right-handed sector

By setting in table (II) \(q_i = q_j = q_k\) and \(n_j = n_k\) the charges of the left-handed fermions become universal, while the right-handed charges are not. This model could be useful since the non-universal sector is singlet under \(SU(2)_L\), hence, we can avoid phenomenological constraints by chosen the right-handed mixing in a convenient way. The Yukawa interaction terms can be chosen as:

\[
\mathcal{L} = \left( q_{Li}^T, \ q_{Lj}^T, \ q_{Lk}^T \right) \begin{pmatrix} y_i^u \tilde{\Phi}_i & y_j^u \tilde{\Phi}_j & y_k^u \tilde{\Phi}_j \\ y_i^d \tilde{\Phi}_i & y_j^d \tilde{\Phi}_j & y_k^d \tilde{\Phi}_j \\ \end{pmatrix} \begin{pmatrix} u_{Ri} \\ u_{Rj} \\ u_{Rk} \end{pmatrix}
\]

\[
+ \left( q_{Li}^T, \ q_{Lj}^T, \ q_{Lk}^T \right) \begin{pmatrix} y_i^d \tilde{\Phi}_i & y_j^d \tilde{\Phi}_j & y_k^d \tilde{\Phi}_j \\ y_i^u \tilde{\Phi}_i & y_j^u \tilde{\Phi}_j & y_k^u \tilde{\Phi}_j \\ \end{pmatrix} \begin{pmatrix} d_{Ri} \\ d_{Rj} \\ d_{Rk} \end{pmatrix}.
\]

The Higgs charges under the new \(U(1)’\) are \(Q_{Z'}(\Phi_i) = n_i + 3q_i\) and \(Q_{Z'}(\Phi_j) = n_j + 3q_j\). This model avoids flavor changing neutral currents in the quark sector associated with non-universal left-handed couplings (non-universal right-handed couplings are not a problem because in these cases the mixing of the right-handed components is not determined by the model and can be chosen in a convenient way). This model has three free parameters which are enough for several applications. With \(\Phi_i\) and \(\Phi_j\) we can also give mass to the lepton sector. So, this model only needs two Higgs doublets to give mass to all standard model fermions.

B. Mixing matrices for 2+1 models

The 2+1 models have identical \(U(1)’\) charges for the \(k, j\) fermion families but allow different charges for the \(i\) family, for these models it is possible to generate the CKM mixing matrix by adding two additional Higgs doublets, \(H^u\) and \(H^d\), coupling to the quark sector in a procedure similar to that outlined in reference [16]. A similar treatment is possible in the lepton sector by adding another couple of Higgs doublets. It is important to notice that one or several scalar fields can acquire a non-zero vacuum expectation value to break the \(U(1)’\) symmetry, so we don’t expect a proliferation of Goldstone bosons. In order to implement the 2+1 models we impose the conditions \(^1 q_i = q_k\) and \(n_j = n_k\) to the \(Z'\) charges in table (II) in such a way that the families \(j\) and \(k\) will have identical charges.

\[
\mathcal{L} = \left( q_{Li}^T, \ q_{Lj}^T, \ q_{Lk}^T \right) \begin{pmatrix} y_i^u \tilde{\Phi}_i & h_{ij}^u \tilde{\Phi}_j & h_{ik}^u \tilde{\Phi}_j \\ 0 & y_j^u \tilde{\Phi}_j & y_k^u \tilde{\Phi}_j \\ 0 & y_i^d \tilde{\Phi}_i & y_k^d \tilde{\Phi}_j \\ \end{pmatrix} \begin{pmatrix} u_{Ri} \\ u_{Rj} \\ u_{Rk} \end{pmatrix}
\]

\[
+ \left( q_{Li}^T, \ q_{Lj}^T, \ q_{Lk}^T \right) \begin{pmatrix} y_i^d \tilde{\Phi}_i & 0 & 0 \\ h_{ij}^d \tilde{\Phi}_j & y_j^d \tilde{\Phi}_j & y_k^d \tilde{\Phi}_j \\ h_{ik}^d \tilde{\Phi}_j & y_k^d \tilde{\Phi}_j & y_k^d \tilde{\Phi}_j \\ \end{pmatrix} \begin{pmatrix} d_{Ri} \\ d_{Rj} \\ d_{Rk} \end{pmatrix}.
\]

The \(Z'\) charges of the additional Higgs doublets are \(Q_{Z'}(H^u) = (n_j + 4q_j - q_i)\) and \(Q_{Z'}(H^d) = n_i + 2q_i + q_j\). According to reference [16] these textures for the quark mass matrices are enough to generate the CKM mass matrix. By Proceeding similarly in the lepton sector, assuming Dirac masses for the neutrinos, it is possible to generate the PMNS matrix adding two Higgs doublets \(H^u\) and \(H^c\) with \(Z'\) charges \(Q_{Z'}(H^u) = n_j + 3q_i\) and \(Q_{Z'}(H^c) = n_i + 6q_i - 3q_j\), respectively. There is also possible to work with Majorana masses under the same assumptions [16]. There are other ways to couple additional scalars to generate the CKM; however, we aim to exemplify the procedure.

\(^1\) Notice that the unique difference respect to the models in the previous section is the condition \(q_i = q_j\)
SM prediction of the cesium, proton, and the electron, hence the corresponding pulls for these observables are the same as those of\(Z\). It is important to emphasize that because the possible constraints come from parity-violation experiments which result from the measurements of the weak charges of the quarks, and a similar expression for neutrinos but using the PMNS matrix. It is useful to define the vector and axial expressions\(Q_{V,A}^{ff}\) for up-type quarks,\(i.e., d, s, b\) we use \(\Delta_{L}^{f}\) \(= g_{Z}^{f} \sum_{f'} \sigma_{f'} \nu_{L}^{f'} v_{L}^{f'} v_{L}^{f'} g_{f'}\) and a similar expression for neutrinos but using the PMNS matrix. It is useful to define the vector and axial expressions\(C_{V,A}^{NP}\) and\(C_{V,A}^{NP}\) respectively, it is possible to obtain a solution with zero couplings to the first family, and avoid contributions of the\(Z'\) boson to the left-handed down and left-handed strange be identical.

Under these restrictions and some other on the absolute value of the charges (see the caption in table IV), we found good fits for\(Z'\) masses below 2.5 TeV (see table V).

The pulls of the observables in table IV are shown in table IV. In order to avoid a best-fit point in the non-perturbative region in the minimization of the\(\chi^{2}\), we restrict the absolute value of the parameters to be less than \(1\) for the second generation and \(3\) for\(l_{3}\) which corresponds to the\(Z'\) left-chiral coupling to the\(\tau\) (except for\(q_{3}\) and\(b_{2}\) which were set at 0.6 and 1.1875, respectively, in order to avoid FCNC constraints and a good fit for the\(C_{9}(\mu)\) and\(C_{10}(\mu)\), simultaneously; however, other choices are possible). By changing these conditions other solutions are possible; however, our aim is to show that it is possible to build a model satisfying all the constraints. It is important to emphasize that because the\(Z'\) couplings to the first family are zero, there is no contribution to the weak charge of the cesium, proton, and the electron, hence the corresponding pulls for these observables are the same as those of SM.

### IV. FLAVOR ANOMALIES AND THE ELECTROWEAK CONSTRAINTS

Part of the aim of this work is to show that it is possible to adjust the flavor anomalies by minimal\(Z'\) models. In order to demonstrate this statement, we carry out a\(\chi^{2}\) analysis including the most relevant constraints on the\(Z'\) parameter space. For models with axial couplings to the electron different from zero \(i.e.,\epsilon_{Z}(e)\neq 0\), important constraints come from parity-violation experiments which result from the measurements of the weak charges of the cesium [64–66], the electron [64, 67] and the proton [64, 68, 69]. Another constraint that only involves left-handed chiral charges derives from the CKM unitarity [70, 71]. This constraint is important since it applies even for models with zero couplings to the quarks.

The\(C_{9}\) and\(C_{10}\) observables, which are involved in the recent discussions about the LHCb anomalies [2, 5–10], have a value different from zero in the SM; our purpose is to include in the analysis the corresponding corrections to these coefficients due to the interaction of the SM fermions with a\(Z'\) gauge boson. These shifts are denoted by\(C_{9}^{NP}\) and\(C_{10}^{NP}\) and are expect to be zero in the SM as indicated in table IV.

We also include constraints coming from neutrino trident production in the scattering of muon neutrino with nuclei. The effective Lagrangian for the new physics involved in this process is \(\mathcal{L}_{\nu_{\mu}\rightarrow \nu_{\mu}A_{\mu}}=-C_{W}^{NP}A_{\mu}^{\nu}p\gamma_{\nu}A_{\mu}\), where \(C_{W}^{NP}\) is the Wilson coefficient at tree level. From this result we obtain a contribution to the neutrino-nucleon scattering like the one shown in the last row in table IV [16, 75].

By choosing \((i,j,k) = (1,2,3)\) in table II and identifying these labels with the charges of the first, second and third family, respectively, it is possible to obtain a solution with zero couplings to the first family, \(i.e., q_{1} = n_{1} = 0\). This choice has a double purpose, first of all, to avoid the strongest constraints from colliders, which are weakened for a\(Z'\) with zero couplings to the up and down quarks, and second, avoid contributions of the\(Z'\) boson to the\(C_{9}(e)\) and\(C_{10}(e)\) coefficients. In order to avoid FCNC, we also impose that the\(Z'\) couplings to the left-handed down and left-handed strange be identical.

### TABLE III: Experimental value and the new physics prediction for the shift in the weak charge of the proton \(Q_{W}(p)\) [68]. Cesium \(Q_{W}(Cs)\) and the electron \(Q_{W}(e)\), owed to the interaction with the \(Z'\). The fourth observable is the constraint on the violation of the first-row CKM unitarity [64, 71]. Constraints on neutrino trident production and the limits on the Wilson coefficients\(C_{9}\) and\(C_{10}\) are also included. For the rotation from the weak basis to the mass eigenstates we adopt the convention [73]:

\[
\Delta_{L}^{f} = g_{Z}^{f} \sum_{f'} \sigma_{f'} \nu_{L}^{f'} v_{L}^{f'} v_{L}^{f'} g_{f'}
\]

with zero couplings to the quarks, and second, avoid contributions of the\(Z'\) boson to the\(C_{9}(e)\) and\(C_{10}(e)\) coefficients. In order to avoid FCNC, we also impose that the\(Z'\) couplings to the left-handed down and left-handed strange be identical.

Under these restrictions and some other on the absolute value of the charges (see the caption in table IV), we found good fits for\(Z'\) masses below 2.5 TeV (see table V).

The pulls of the observables in table IV are shown in table IV. In order to avoid a best-fit point in the non-perturbative region in the minimization of the\(\chi^{2}\), we restrict the absolute value of the parameters to be less than \(1\) for the second generation and \(3\) for\(l_{3}\) which corresponds to the\(Z'\) left-chiral coupling to the\(\tau\) (except for\(q_{3}\) and\(b_{2}\) which were set at 0.6 and 1.1875, respectively, in order to avoid FCNC constraints and a good fit for the\(C_{9}(\mu)\) and\(C_{10}(\mu)\), simultaneously; however, other choices are possible). By changing these conditions other solutions are possible; however, our aim is to show that it is possible to build a model satisfying all the constraints. It is important to emphasize that because the\(Z'\) couplings to the first family are zero, there is no contribution to the weak charge of the cesium, proton, and the electron, hence the corresponding pulls for these observables are the same as those of SM.

| \(\mathcal{O}\)                     | Value [64, 68, 72] | SM prediction \(\mathcal{O}_{SM}\) [64] | \(\Delta\mathcal{O} = \mathcal{O} - \mathcal{O}_{SM}\) |
|-----------------------------------|--------------------|------------------------------------------|-----------------------------------------------------|
| \(Q_{W}(p)\)                      | 0.0719 ± 0.0045    | 0.0708 ± 0.0003                         | 4 \(\frac{M_{W}^{2}}{91.1875}\) \(\Delta_{L}^{e} (2\Delta v^{u} + \Delta d^{d})\) |
| \(Q_{W}(Cs)\)                     | -72.62 ± 0.43      | -73.25 ± 0.02                           | \(Z\Delta Q_{W}(p) + N \Delta Q_{W}(n)\)            |
| \(Q_{W}(e)\)                      | -0.0403 ± 0.0053   | -0.0473 ± 0.0003                        | 4 \(\frac{M_{W}^{2}}{91.1875}\) \(\Delta_{L}^{e} \Delta v^{e}\) |
| \(1 - \sum_{q=d,s,b} |V_{eq}|^2\)     | 1 - 0.9999(6)      | 0                                       | \(\frac{3}{4\pi} \frac{M_{W}^{2}}{M_{Z}^{2}} \Delta_{L}^{e} (\Delta v^{e} - \Delta d^{d})\) |
| \(C_{V}^{NP}(\mu)\)              | -1.29^{+0.21}_{-0.20} | 0                                      | \(-\frac{1}{2\pi} \frac{M_{W}^{2}}{M_{Z}^{2}} \Delta_{L}^{e} \Delta v^{e}\) |
| \(C_{A}^{NP}(\mu)\)              | +0.79^{+0.26}_{-0.24} | 0                                      | -\(\frac{5}{2\pi} \frac{M_{W}^{2}}{M_{Z}^{2}} \Delta_{L}^{e} \Delta v^{e}\) |
| \(\sum_{SM+Z'} \sigma_{SM} \)    | 0.83 ± 0.18        | 1                                       | \(1 + (1+4g_{Z})^{2} \Delta v^{e} / (2M_{Z}^{2})^{2} - 1\) |
TABLE IV: Pulls for low energy experiments in the $\chi^2$ minimization for a $M_{Z'} = 2.5$ TeV. In this analysis we identify $i = 1, 2, 3$ with the first, second and third generation of fermions, respectively. The minimization was carried out by imposing the constraints $q_1 = q_2$, and $q_1 = u_1 = d_1 = 0$, in order to avoid FCNC and LHC constraints, respectively. This choice has a double purpose since it forbids any contribution of the $Z'$ to $C_{9}(e)$ and $C_{10}(d)$ which involve fermions of the first family. To evade too large lepton couplings, in order to avoid non-perturbative charges, in the second and third family we restrict the $Z'$ couplings of the SM fermions of the second and third families to have an absolute value smaller than 1 and 3, respectively (except for $q_3$ and $l_3$ which were set at 0.6 and 1.1875, respectively, in order to avoid FCNC constraints and a good fit for the $C_9(\mu)$ and $C_{10}(\mu)$, simultaneously; however, other choices are possible). We did not impose any constraint on the right-handed neutrino couplings $n_i$ due to the absence of constraints on these parameters. For the minimization of the $\chi^2$ we restrict the absolute value of the parameters to be less than 1 for the second generation, and 3 for $l_3$ which corresponds to the $Z'$ left-chiral coupling to the $\tau$. Another sets of charges are also possible by changing these constraints.

\[
\begin{array}{|c|c|c|c|c|c|c|}
\hline
\text{Pull}' = \frac{C_{\text{exp}}^i - C_{\text{th}}^i}{\sqrt{\sigma^2_{\text{exp}} + \sigma^2_{\text{th}}}} & \text{Pull} & \text{Pull} & \text{Pull} & \text{Pull} & \text{Pull} & \text{Pull} \\
\hline
O^i & Q_W(p) & Q_W(Cs) & Q_W(e) & \text{CKM} & C_9 & C_{10} & \nu\text{-Trident} & \chi^2_{\text{min}} \\
\hline
0.244 & 1.46 & 1.38 & -1.10 & -0.575 & 0.700 & -1.00 & 7.13 \\
\hline
\end{array}
\]

TABLE V: Best fit values for the $Z'$ chiral charges of SM fermions, right-handed neutrinos and the Higgs doublets. $i = 1, 2, 3$ correspond to the first, second and third generation of fermions.

In figure 1 the 95% CL allowed regions for several observables are shown. It is important to stress that a similar plot exists between any couple of parameters of the model. For this reason it is difficult to obtain general conclusions from this figure; however, the plot serves to get some idea about how each observable put constraints on the parameter space. These parameters, $n_2$ and $q_1$, are important owing that they are related to the observables of our analysis, $n_2$ appears in all the charges of the second family except in the $Z'$ coupling of the right-handed muon. $q_1$ corresponds to the $Z'$ coupling of the left-handed up and down quark and the $Z'$ coupling of the left-handed electron is also proportional to this parameter. The latter is important for the collider constraints \[62, 77–80\].

For the time being, the strongest constraints come from the proton-proton collisions data collected by the ATLAS experiment at the LHC with an integrated luminosity of 36.1 fb$^{-1}$ at a center of mass energy of 13 TeV \[81\]. In particular, we used the upper limits at 95% C.L. on the total cross-section of the $Z'$ decaying into dileptons (i.e., $e^+e^-$ and $\mu^+\mu^-$). Figure 1 shows the contours in the parameter space of the minimal models at 95% C.L. for $M_{Z'} = 2.5$ TeV. We obtain these limits from the intersection of $\sigma^{\text{NLO}}(pp \rightarrow Z' \rightarrow l^+l^-)$ with the ATLAS 95% C.L. upper limits on the cross-section (for additional details see reference \[82\]). As a cross-check we calculated these limits for the sequential SM and some $E_6$ models finding the same value than that reported by the collaboration \[80\].

A. Flavor changing neutral currents

We assume zero mixing between the $Z$ and $Z'$ \[2\], in such a way that all the constraints proportional to the $Z$-$Z'$ mixing angle $\theta_{Z'Z}$ in section 3.7 in the classical paper of Langacker and Plumacher \[83\] are satisfied automatically. The constraint coming from $\mu$-$e$ conversion in a muonic atom has two contributions (Eq. (22) in reference \[83\]) , one
FIG. 1: Colored regions correspond to the allowed parameter space at the 95% C.L for a $M_{Z'} = 2.5$ TeV. The region enclosed between the black-dashed lines corresponds to the 95% C.L. allowed parameter space by the cesium weak charge measurements [64–66, 76]. The yellow region corresponds to the 95% C.L. allowed parameter space by the electron weak charge measurements in Moller scattering [64, 67]. The green region corresponds to the 95% C.L. allowed parameter space by the proton weak charge measurements [68]. The region enclosed between the orange-dot-dashed lines corresponds to the 95% C.L. allowed parameter space by the constraints on the violation of the first-row CKM unitarity [70, 71]. By combining all the low energy data considered in our analysis the 95% C.L. allowed parameter space corresponds to the red region. The cyan and magenta regions correspond to the 95% C.L. parameter spaces consistent with the best fit values for the $C_9$ and $C_{10}$, respectively. The blue region corresponds to the 95% C.L. parameter space allowed by data from proton-proton collisions decaying to $\mu$ pairs in the ATLAS detector for an integrated luminosity of $36.1 \text{ fb}^{-1}$ at a center of mass energy of 13 TeV.

It is important to stress that there is a lot of freedom in the choice of these parameters. Our purpose is to show that under some reasonable assumptions it is possible to build a model. It is important to mention that an update of the reference [83] is necessary in order to include the latest measurements of the kaon properties [84, 85].
V. CONCLUSIONS

In this work we presented an anomaly-free non-universal $Z'$ family of models, which only includes SM fermions plus right-handed neutrinos and two Higgs doublets. Our solutions have three families with different charges for every family, i.e., the model is non-universal; however, a priori it is not possible to identify one of them with a particular family in the SM; hence, it is necessary a study of the phenomenology of all the possibilities.

By means of an explicit example, we show that it is possible to build a model with zero couplings to the up and down quarks and in general to the fermions of the first family, in such a way that the model evades collider constraints and does not contribute to the corresponding the Wilson coefficients $C_9(e)$ and $C_{10}(e)$. Simultaneously, our solution is flexible enough to accommodate the flavor anomalies in the Wilson coefficients $C_9(\mu)$ and $C_{10}(\mu)$. By requiring that the left-handed couplings of the down and strange couplings be identical it is possible to avoid FCNC.

What follows is to analyze the constraints for a $Z'$ with strong couplings to the $\mu$ and $\tau$ leptons but zero couplings to the up and down quarks [17].

Acknowledgments

R. H. B. and L. M. thank the “Centro de Investigaciones ITM”. We thank Financial support from “Patrimonio Autónomo Fondo Nacional de Financiamiento para la Ciencia, la Tecnología y la Innovación, Francisco José de Caldas”, and “Sostenibilidades UDEA”. This research was partly supported by the Vicerrectoría de Investigaciones, Posgrados y Relaciones Internacionales (VIPRI) de la Universidad de Nariño, project numbers 1928 and 2172.

[1] R. Pohl et al., Nature 466, 213 (2010). doi:10.1038/nature09250
[2] R. Aaij et al. [LHCb Collaboration], Phys. Rev. Lett. 111, 191801 (2013) doi:10.1103/PhysRevLett.111.191801 [arXiv:1308.1707 [hep-ex]].
[3] A. J. Krasznahorkay et al., Phys. Rev. Lett. 116, no. 4, 042501 (2016) doi:10.1103/PhysRevLett.116.042501 [arXiv:1504.01527 [nucl-ex]].
[4] A. Heister, arXiv:1610.06536 [hep-ex].
[5] R. Aaij et al. [LHCb Collaboration], JHEP 1406, 133 (2014) doi:10.1007/JHEP06(2014)133 [arXiv:1403.8044 [hep-ex]].
[6] R. Aaij et al. [LHCb Collaboration], Phys. Rev. Lett. 113, 151601 (2014) doi:10.1103/PhysRevLett.113.151601 [arXiv:1406.6482 [hep-ex]].
[7] R. Aaij et al. [LHCb Collaboration], JHEP 1602, 104 (2016) doi:10.1007/JHEP02(2016)104 [arXiv:1512.04442 [hep-ex]].
[8] S. Wehle et al. [Belle Collaboration], Phys. Rev. Lett. 118, no. 11, 111801 (2017) doi:10.1103/PhysRevLett.118.111801 [arXiv:1612.05014 [hep-ex]].
[9] R. Aaij et al. [LHCb Collaboration], JHEP 1307, 084 (2013) doi:10.1007/JHEP07(2013)084 [arXiv:1305.2168 [hep-ex]].
[10] R. Aaij et al. [LHCb Collaboration], JHEP 1509, 179 (2015) doi:10.1007/JHEP09(2015)179 [arXiv:1506.08777 [hep-ex]].
[11] A. Vicente, Adv. High Energy Phys. 2018, 3905848 (2018) doi:10.1155/2018/3905848 [arXiv:1803.04703 [hep-ph]].
[12] B. Allanach, F. S. Queiroz, A. Strumia and S. Sun, Phys. Rev. D 93, no. 5, 055045 (2016) Erratum: [Phys. Rev. D 95, no. 11, 119902 (2017) doi:10.1103/PhysRevD.95.119902 [arXiv:1511.07447 [hep-ph]].
[13] W. Altmannshofer, S. Gori, S. Profumo and F. S. Queiroz, JHEP 1612, 106 (2016) doi:10.1007/JHEP12(2016)106 [arXiv:1609.04926 [hep-ph]].
[14] J. Ellis, M. Fairbairn and P. Tunney, Eur. Phys. J. C 78, no. 3, 238 (2018) doi:10.1140/epjc/s10052-018-5725-0 [arXiv:1705.03447 [hep-ph]].
[15] S. Baek, Phys. Lett. B 781, 376 (2018) doi:10.1016/j.physletb.2018.04.012 [arXiv:1707.04573 [hep-ph]].
[16] L. Bian, S. M. Choi, Y. J. Kang and H. M. Lee, Phys. Rev. D 96, no. 7, 075036 (2017) doi:10.1103/PhysRevD.96.075038 [arXiv:1707.04811 [hep-ph]].
[17] M. Abdulliah, M. Dalchenko, B. Dutta, R. Eusebi, P. Huang, T. Kamon, D. Rathjens and A. Thompson, Phys. Rev. D 97, no. 7, 075035 (2018) doi:10.1103/PhysRevD.97.075035 [arXiv:1707.07016 [hep-ph]].
[18] G. Faisel and J. Tandean, JHEP 1802, 074 (2018) doi:10.1007/JHEP02(2018)074 [arXiv:1710.11102 [hep-ph]].
[19] A. K. Alok, B. Bhattacharya, D. Kumar, J. Kumar, D. London and S. U. Sankar, Phys. Rev. D 96, no. 1, 015034 (2017) doi:10.1103/PhysRevD.96.015034 [arXiv:1703.09247 [hep-ph]].
[20] J. Ellis, M. Fairbairn and P. Tunney, arXiv:1807.02503 [hep-ph].
[21] V. Barger, L. L. Everett, J. Jiang, P. Langacker, T. Liu and C. E. M. Wagner, JHEP 0912, 048 (2009) doi:10.1088/1126-6708/2009/12/048 [arXiv:0906.3745 [hep-ph]].
[22] X. G. He, G. C. Joshi, H. Lew and R. R. Volkas, Phys. Rev. D 43, 22 (1991). doi:10.1103/PhysRevD.43.22
[23] X. G. He, G. C. Joshi, H. Lew and R. R. Volkas, Phys. Rev. D 44, 2118 (1991). doi:10.1103/PhysRevD.44.2118
[24] T. Appelquist, B. A. Dobrescu and A. R. Hopper, Phys. Rev. D 68, 035012 (2003) doi:10.1103/PhysRevD.68.035012 [hep-ph/0212073].
[65] C. S. Wood, S. C. Bennett, D. Cho, B. P. Masterson, J. L. Roberts, C. E. Tanner and C. E. Wieman, Science 275, 1759 (1997). doi:10.1126/science.275.5307.1759

[66] J. Guena, M. Lintz and M. A. Bouchiat, Phys. Rev. A 71, 042108 (2005) doi:10.1103/PhysRevA.71.042108 [physics/0412017 [physics.atom-ph]].

[67] D. Androic et al. [Qweak Collaboration], Phys. Rev. Lett. 95, 081601 (2005) doi:10.1103/PhysRevLett.95.081601 [hep-ex/0504049].

[68] A. Anastasi et al. [KLOE-2 Collaboration], JHEP 1809, 021 (2018) doi:10.1007/JHEP09(2018)021 [arXiv:1806.08654 [hep-ex]].