Interpretable Representation Learning for Speech and Audio Signals Based on Relevance Weighting

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Abstract—The learning of interpretable representations from raw data presents significant challenges for time series data like speech. In this work, we propose a relevance weighting scheme that allows the interpretation of the speech representations during the forward propagation of the model itself. The relevance weighting is achieved using a sub-network approach that performs the task of feature selection. A relevance sub-network, applied on the output of first layer of a convolutional neural network model operating on raw speech signals, acts as an acoustic filterbank (FB) layer with relevance weighting. A similar relevance sub-network applied on the second convolutional layer performs modulation filterbank learning with relevance weighting. The full acoustic model consisting of relevance sub-networks, convolutional layers and feed-forward layers is trained for a speech recognition task on noisy and reverberant speech in the Aurora-4, CHiME-3 and VOiCES datasets. The proposed representation learning framework is also applied for the task of sound classification in the UrbanSound8K dataset. A detailed analysis of the relevance weights learned by the model reveals that the relevance weights capture information regarding the underlying speech/audio content. In addition, speech recognition and sound classification experiments reveal that the incorporation of relevance weighting in the neural network architecture improves the performance significantly.

Index Terms—Deep Representation Learning, Relevance Modeling, Raw Waveform Processing, Modulation Filtering, Acoustophonetics, Automatic Speech Recognition, Urban Sound Classification.

I. INTRODUCTION

Representation learning is the branch of machine learning that comprises of the methods that allow the learning of meaningful representations from raw data. With the growing interest in deep learning, representation learning using deep neural networks has been actively pursued [1]. The modalities like text and image have shown important successes for representation learning methods (for example, using word2vec models [2]). However, representation learning for speech data has been more challenging due to the temporal and intrinsic variabilities of the signals. Due to these challenges, the most common representation used in state-of-art speech recognition systems continues to be the mel spectrogram. In this paper, we explore representation learning for speech directly from the raw-waveform using a novel modeling approach.

The broad set of representation learning works in the speech domain can be categorized as supervised and unsupervised. In supervised setting, the main direction pursued has been the learning of the acoustic filterbank parameters from raw waveforms [3]–[5]. Compared to the acoustic models using the mel spectrogram features, these models are fed with raw speech signal and the first layer of the acoustic model performs a time-frequency decomposition of the signal. The supervised objective function is either a detection or a classification task [4], [6], [7]. In many of these cases, the initialization of the acoustic filter bank parameters are done using gammatone filters that closely approximate the hearing periphery [5]. [7]. However, in spite of many of these efforts, the filter learning from raw waveform has not yielded performance improvements over the mel spectrogram features [3], [7].

For unsupervised learning of acoustic representations, Sailor et al. [8] investigated the use of restricted Boltzmann machines while Agrawal et al. [9] explored variational autoencoders. The wav2vec method proposed in [10] explored unsupervised pre-training for speech recognition by learning representations of raw audio. In our previous work, we had also explored modulation filter learning using an unsupervised objective function [11]. The approach of self-supervised learning (similar to the word2vec models for text) has also been pursued by Pascual et. al [12]. A comparison of several neural network architectures for modulation filter learning was also explored in [13].

In many of these previous approaches, the learned representations are assumed to capture distinctive speech features for phonetic discrimination. However, there has been limited attempts to explore the interpretability of the learned filterbanks. One exception is the SincNet filterbank [14] where the authors showed that the filter learning is resilient to the presence of band-limited noise. However, compared to vector representations of text which have shown to embed meaningful semantic properties, the interpretability of speech representations has been limited.

In this paper, we propose a relevance weighting mechanism that allows the interpretability of the learned representations in the forward propagation itself. The term “relevance weighting” comes from the text domain, where a static relevance weight is attached to each document, based on the relevance to the search term feature [15], [16]. A similar application of visual attention in the image domain uses spatial weighting to weight different parts of the image [17]. In this work, the term relevance weighting refers to the scheme of automatic weighting of the learned representations using a sub-network.

The proposed model consists of a two-step relevance
weighting approach. The first step performs relevance weighting on the output of the first layer of convolutions. This convolutional layer learns a parametric acoustic filterbank from the raw waveform. The relevance weighted filterbank representation is used as input to the second convolutional layer which performs modulation filtering. This layer repeats the operations of the first layer in a 2-D fashion. The kernels of the second convolutional layer are 2-D spectro-temporal modulation filters and the filtered representations are weighted using another relevance sub-network. The rest of the neural network architecture performs the task of acoustic modeling for speech recognition. All the model parameters including the acoustic layer parameters, acoustic filterbank relevance sub-network, modulation filters and modulation relevance sub-network are learned in a supervised learning paradigm.

The subsequent analysis of the relevance sub-network reveals that the weights from the network contain information regarding the phonetic content of the label. The relevance weights are also adaptive to the presence of noise in the data. The automatic speech recognition (ASR) experiments are conducted on Aurora-4 (additive noise with channel artifact), CHiME-3 (additive noise with reverberation) and VOiCES (additive noise with reverberation) datasets. These experiments show that the learned representations from the proposed framework provide considerable improvements in ASR results over the baseline methods. The proposed representation learning framework is further extended to the task of urban sound classification (USC) on the Urbansound8K dataset where the goal is to classify short audio snippets into 10 urban sound classes. In this task, the proposed approach shows improved classification performance and the weight analysis reveals distinctive audio characteristics that are captured by the relevance weighting scheme.

The rest of the paper is organized as follows. Section II details the motivation and related work. Section III describes the proposed two-step representation learning approach using relevance weighting. This is followed by interpretability analysis of the proposed representation learning in Section IV. Section V describes the ASR experiments with the various front-ends. The discussion of the model is given in Section VI. This is followed by a summary in Section VII.

II. MOTIVATION AND RELATED WORK

One of the major motivations for the proposed modeling approach of relevance weighting is the evidence of gain enhancement mechanism in human sensory system. Both physiological and behavioral studies have suggested that stimulus-driven neural activity in the sensory pathways can be modulated in amplitude with attention. The recordings of event-related brain potentials indicate that such sensory gain control or amplification processes play an important role in tasks that involve attention. The combined event-related brain potential and neuroimaging experiments provide strong evidence that attentional gain control operates at an early stage of sensory processing. These evidences support feature selection theories of attention and provide a basis for distinguishing between separate mechanisms of attentional suppression (of unattended inputs) and attentional facilitation (of attended inputs).

The second motivation comes from prior works on Mixture of Experts (MoE) models. For neural networks the work proposed by Shazeer et al. explored multiple parallel neural networks followed by a gating network which performs a combination of the outputs from the networks. This MoE model showed significant promise for a language modeling task. The self attention module successfully inducted in transformer models also incorporates information from multiple streams using a linear combination.

Inspired by these human and machine learning studies, the proposed relevance weighting attempts to model gain enhancement in a neural architecture. The frequency selectivity observed in auditory system can be modeled as relevance weighting in the acoustic filter bank layer while the cortical layer gain enhancement is attempted by modulating the relevance weights of the modulation filtering layer. While attention and MoE models attempt a combination of input streams that are fed to successive layers, the proposed relevance weighting merely performs a gain enhancement without a linear combination.

The learning of acoustic filterbank from raw waveform has been actively pursued in the last few years. The work reported by Palaz et al. proposed the use of convolutional neural networks on raw waveform to estimate phoneme class conditional probabilities. Similarly, Sainath et al. used power spectrum as input to convolutional neural network (CNN) to learn the filterbank features. For learning interpretable representations, the authors in used Gaussian functions instead of mel-scale filterbanks with input being power spectra. The work proposed in initializes the convolutional filters with Gabor wavelets before proceeding to learn the filter parameters. Ravanelli et al. showed the use of sinc filters as parametric filters, with only the lower and higher cutoff frequencies learned from data. This work is extended in to learn filterbank representations in a self-supervised framework.

The approach of modulation filter learning (modulation filters process the time-frequency representation as a 2-D image and perform filtering along time (rate) and frequency (scale) dimensions) using the linear discriminant analysis (LDA) has also been explored to learn the temporal modulation filters in a supervised manner. There have also been attempts to learn modulation filters in an unsupervised manner.

The performance of the learned representations from previous efforts has often been comparable to the mel-spectrogram features. However, most of the previous attempts do not allow the interpretation of the learned representations or their ability to capture relevant information.

III. RELEVANCE WEIGHTING BASED REPRESENTATION LEARNING

The block schematic of the proposed relevance weighting based representation learning is shown in Figure 1.

A. Acoustic Filterbank Learning with Relevance Weighting

The first layer of the proposed model performs acoustic filtering from the raw waveforms using a convolutional layer.
The input to the neural network are raw samples windowed into \( s \) samples per frame. This frame of raw audio samples are processed with a 1-D convolution using \( f \) kernels each of size \( k \). The kernels are modeled using a cosine-modulated Gaussian function [9].

\[
g_i(n) = \cos 2\pi \mu_i n \times \exp \left( -n^2 \mu_i^2 / 2 \right)
\]

where \( g_i(n) \) is the \( i \)-th kernel (\( i = 1, \ldots, f \)), \( \mu_i \) is the center frequency (mean parameter) of the \( i \)-th kernel. The parametric approach to filterbank (FB) learning generates filters with a smooth frequency response. The Gaussian window has interesting properties of being smooth in time and frequency domain. In order to preserve the positive range of frequency a smooth frequency response. The Gaussian window has been found to be sufficient to capture temporal variations of the acoustic feature maps. These outputs are squared, average pooled within each frame and log transformed.

### 1) Relevance weighting

The relevance weighting paradigm for acoustic FB layer is implemented using a relevance sub-network. This network is fed with the acoustic feature map of dimension \( 1 \times t \) for each of the \( f \) Gaussian kernel (each row of the time-frequency representation \( x \)). A two layer deep neural network (DNN) with a \( t \) dimensional input layer and a scalar output realizes the relevance sub-network. This operation is repeated for all the \( f \) acoustic feature maps to generate \( x_a \) as a \( f \) dimensional vector with weights corresponding to each kernel. The relevance weights \( w_a \) are generated using the softmax function as,

\[
w_a^i = \frac{e^{x_a^i}}{\sum_j e^{x_a^j}} \quad \text{where} \quad i = 1, 2, \ldots, f.
\]

The weights \( w_a \) are multiplied with each of the acoustic feature map (rows of \( x \)) to obtain the relevance weighted time-frequency representation \( y \). The relevance weights in the proposed framework are different from typical attention mechanism [32]. In the proposed framework, relevance weighting is applied over the representation as soft feature selection weights without a linear combination as done in attention models [32].

We also smooth the first stage outputs (weighted spectrogram \( y \) of length \( t \) time frames) using a normalization method inspired by instance norm principle [33]. Let \( y_{j,i} \) denote the relevance weighted time-frequency representation for frame \( j \) \((j = 1, \ldots, t)\) of kernel \( i \) \((i = 1, \ldots, f)\). The soft weighted output \( z_{j,i} \) is given as,

\[
z_{j,i} = \frac{y_{j,i} - m_i}{\sqrt{\sigma_i^2 + c}}
\]

where \( m_i \) is the sample mean of \( y_{j,i} \) computed over \( j \) and \( \sigma_i \) is the sample std. dev. of \( y_{j,i} \) computed over \( j \). The constant \( c \) acts as a relevance factor and is chosen as \( 10^{-4} \). The output of relevance weighting \( z \) is propagated to the subsequent layers for the acoustic modeling.

In our experiments, we use \( t = 101 \) whose center frame is the senone target for the acoustic model. We also use \( f = 80 \) kernels each of length \( k = 129 \). This value of \( k \) corresponds to 8 ms in time for a 16 kHz sampled signal which has been found to be sufficient to capture temporal variations of...
a speech signal [35]. The value of $s$ is 400 corresponding to a 25ms window length and the frames are shifted every 10ms. The instance norm is not applied globally but rather applied on the given input patch of $t = 101$ time frames (shown in Fig. 1). This corresponds to 1-second of length approximately. In our experiments, we also find that, after the normalization layer, the number of frames $t$ can be pruned to the center 21 frames for the acoustic model training without loss in performance. This has significant computational benefits and the pruning is performed to keep only the 21 frames around the center frame.

Figure 2 shows the center frequency ($\mu_i$ values sorted in ascending order) of the acoustic filters obtained using multi-condition Aurora-4 (noisy) and CHiME-3 (noise and reverberations) datasets (details of the datasets are given in Section V) and this is compared with the center frequency of the conventional mel filterbank [36]. As can be observed, the proposed filterbank allocates more filters in lower frequencies compared to the mel filterbank. The CHiME-3 data contains reverberation artifacts which resulted in lower center frequencies than the noisy Aurora-4 data center frequency values.

The soft relevance weighted time-frequency representation $z$ obtained from the proposed approach is shown in Figure 3 for an utterance with airport noise from Aurora-4 dataset (the waveform is plotted in Figure 3(a)). The corresponding mel spectrogram (without relevance weighting) is plotted in Figure 3(b). The time-frequency representation obtained through the learned filterbank (without relevance weighting) is plotted in Figure 3(c). It can be observed that, in the learned filterbank representations (Figure 3(c) and (d)), the formant frequencies are shifted upwards because of the increased number of filters in the lower frequency region. Also, the relevance weighting modifies the representations to preserve only the important details of the spectrogram.

**B. Modulation Filterbank Learning with Relevance Weighting**

The representation $z$ from acoustic filterbank layer is fed to the second convolutional layer which is interpreted as modulation filtering layer (shown in Figure 1). Specifically, the modulation filter is characterized using the rate (temporal variations measured in Hz) and scale (spectral variations measured in cyc. per octave) dimensions. The first layer (acoustic FB) generates time-frequency representations (2-D representations) as the output ($z$ in Fig. 1). These 2-D representations are indexed by time-frame on x-direction and sub-band index in the y-direction. The sub-band indices are ordered in increasing order of center frequency which is required for modulation filtering in the second layer. The next stage of 2-D modulation filtering (rate-scale) is applied on 2-D time-frequency representation. The column of the time-frequency representation from the first layer constitutes a warped sampling of the spectrum from $0 - 8$ kHz with center frequencies shown in Figure 2. Hence, applying a filter along the y-direction of this 2-D time frequency representation constitutes scale filtering and the application of the filter along the x-direction constitutes rate filtering. Note that the sampling in the y-direction is non-linear in frequency.

In this work, we explore parametric and non-parametric approaches to modulation filter learning. In the parametric approach, the modulation filterbank (kernels of the modulation convolution layer) is designed as 2-D cosine-modulated Gaussian filters. Here, the $i$th 2-D filter $g_i$, with rate frequency $\mu_r$, and scale frequency $\mu_s$, is designed as:

$$g_i(a,b) = \cos 2\pi(\mu_r a \pm \mu_s b) \times \exp \left[ (-a^2) + (-b^2) \right]$$

with $a$ sampled at 100 Hz (corresponding to 10 ms hop in the time-frequency representation), $b$ sampled at 24 cyc. per octave, and $i = 1, ..., K$ for $K$ modulation filters. The $\pm$ sign in the cosine term is used to incorporate upward and downward moving patterns in the input time-frequency representation. The cosine frequencies $\mu_{r_i}$ and $\mu_{s_i}$ are interpreted as rate and scale center frequencies in 2-D frequency response of the modulation filter. The means are the learnable parameters of the 2-D kernels and these are learned jointly with rest of the network parameters. We learn $K = 40$ modulation feature maps using kernels of $5 \times 5$ filter tap size.

The learned center frequencies $\mu_r$ and $\mu_s$ (rate-scale) of the modulation filters are shown in Figure 4 from a model trained using Aurora-4 database. The rate frequency values span up to 50 Hz, while the scale frequency can span from 0 to 12 cycles/octave. It can be observed from the plot that the learned filters span the rate-scale space with more density till around 35 Hz rate frequency. The learned center frequencies span low scale regions with most of the filters in the $[-2, 6]$ cyc. per octave range. We begin with randomly spaced grid of rate-scale values (center frequency) as initialization and let the network update the center frequency values. The modulation feature maps $p$ are pooled, leading to feature maps of size $f' \times t'$. These are weighted using a second relevance weighting sub-network (referred to as the modulation filter relevance sub-network in Figure 1). The input to the modulation relevance weighting sub-network is a modulation feature map of size $f' \times t'$ and the model generates a scalar value for each of the $K$ feature maps. Let $p_m$ denote the $K$ dimensional vector from the output of modulation relevance sub-network. Similar to the acoustic relevance network, a softmax function is applied to
The proposed two stage processing is loosely modeled based on our understanding of the human auditory system, where the cochlea performs acoustic frequency analysis while early cortical processing performs modulation filtering \[39\]. The relevance weighting mechanism attempts to model the feature selection/weighting inherently present in the auditory system (based on the relative importance of the representation for the downstream task).

IV. INTERPRETABILITY OF THE REPRESENTATIONS

We analyze the representations and the relevance weights (outputs of acoustic relevance sub-network and modulation relevance sub-network) learned by the proposed model. The model architecture, shown in Figure 1, is trained using the Aurora-4 dataset. This model is tested using the TIMIT dataset (without any retraining). We use clean TIMIT as well as TIMIT dataset corrupted with noise \[40\]. The TIMIT dataset is hand labelled for phonemes, which allows the interpretation of the model representations based on the phoneme identity. For the analysis, the noisy TIMIT test set consisting of 1344 utterances is corrupted with 4 different noise conditions, namely babble, exhall, restaurant and subway at 2 different SNR levels, 0 dB and 20 dB SNR.

The phonemes are analyzed in two groups. A group of vowel phonemes \{/ao/, /aad/, /ael/, /eyl/, /iy/, /uw/\} and a group of consonants from 3 categories: plosives \{/th/\}, fricatives \{/sh/, /zh/\}, and nasals \{/m/, /em/, /eng/\}. The vowel sounds are also organized from back to front with regard to the place of articulation \[41\].

A. Mean Time-Frequency Representations

We analyze the learned time-frequency representation of each phoneme from the first layer (using the representation \(x\) with 7 previous and 7 succeeding frames that cover 165 ms duration). For example, the time-frequency representation of all /aa/ vowel exemplars (denoted as \(x\) in Figure 1) are extracted from TIMIT utterances and are averaged to obtain one average time-frequency representation, as shown in Figure 6 (top row second column). For the computation of the average spectrogram for each phoneme, a contextual window of +/−7 frames are chosen around the center frame (from every exemplar of that phoneme occurrence in the files) irrespective of the phone duration. Thus, all center frames belonging to a phoneme, except the two boundary frames on either side, are
used in computing the average time-frequency representation of Figure 6.

The averaged time-frequency representation learned by the model reveals that mid/back vowels \{/ao/, /aa/, /ae/\} have relatively more concentrated activity at low to medium frequencies (0.5 – 2 KHz), whereas front vowels \{/ey/, /iy/\} have two distinct peaks spaced over a larger frequency range around 0.3 and 4 KHz respectively. This is consistent with the known distribution of the three formants F1, F2, and F3 in these vowels [4]. On the other hand, while the plosive /t/, being a stop-consonant, has a time varying profile, the fricatives \{/sh/, /zh/\} have dominant energy at high frequencies and the nasal sounds \{/m/, /em/\} have energy at low to mid frequencies. Thus, the early representations learned by the model attempt to capture distinct phonetic properties. The purpose of this analysis is to relate the relevance weight plots that are analyzed in the following sections to the phonetic properties of the time-frequency representation.

B. Acoustic FB Relevance Weights

The acoustic filterbank relevance weights \(w_a\) are analyzed to understand the weighting incorporated through the relevance sub-network. The relevance weights are averaged across the utterances for each phoneme and SNR level separately. Figure 7 shows the relevance weights for clean data and noisy data averaged over all the 4 noise types.

As can be observed for clean and SNR of 20 dB (low noise), for the front vowels \{/ey/, /iy/, /uw/\}, the filter indices that have the higher relevance weights lie in 500 – 600 Hz range. For the mid/back vowels \{/ao/, /aa/, /ae/\}, more relevance is seen in the filter indices having center frequency above 800 Hz. The filter indices with the highest relevance weights (peak marked with black star in Figure 7) tend to shift towards lower frequency as we move from the back vowel /ao/ to the front vowel /uw/. This is also very similar to the filter representations seen in the auditory system of ferrets and other mammals [41]. Also, in front/closed vowels \{/iy/, /uw/\}, the relevance weights show a second peak at the higher frequency index due to the presence of a higher formant frequency F3 (in the center frequency range of 3.5 – 4 KHz). For the high noise condition (SNR 0 dB), the relevance weights still preserve some of the phoneme specific selectivity although the weights tend to become more uniform across the frequency range. A more closer look at the relevance weights is given in Figure 8 where 3 vowels are analyzed in clean conditions. As seen here, the peak activity moves from 800Hz to 500Hz as we move from back vowels to front vowels.

The acoustic filterbank (FB) relevance weights for consonants is shown in the second row of Figure 7. The plosive /t/ shows similar relevance weighting as observed in front vowels. The fricatives \{/sh/, /zh/\} show lesser sub-band selectivity compared to other phonemes (as these phonemes have significant high frequency activity as seen in Figure 6). The nasal sounds \{/m/, /em/\} also elicit a large range of filter indices that have high relevance weights. Similar to the vowels, the decrease in SNR (higher noise case) reduces the selectivity of the representations as the relevance weights become more uniform. This is again similar to the human auditory processing where noise segregation happens to a very small degree in the peripheral time-frequency representation as compared to higher auditory cortical areas [42].
The normalized acoustic FB relevance weight profile for each phoneme: vowels in top row and consonants in bottom row, computed using the relevance weights for clean (black dotted) and noisy TIMIT files with SNR 20 dB (black solid) and SNR 0 dB (red dot-dashed), respectively.

Fig. 8. Vowel Analysis - Acoustic filterbank (FB) relevance weights for 3 vowels on clean TIMIT data (black dotted curve for vowels in Figure 7). This figure highlights the contrast among vowels for clean condition.

C. Modulation Filtering With Relevance Weighting

Figure 7 shows the bubble plot for modulation filter relevance weights for different phonemes (averaged over all respective exemplars of each phoneme). This plot is obtained by placing the relevance weight at the location of the center frequency (rate-scale) of the corresponding modulation filter. The size of the bubble is proportional to the magnitude of the corresponding relevance weight. The vowels and consonants are arranged in the same order as in acoustic FB relevance weight analysis. In order to highlight the contrast, we plot relevance weights for a given phoneme after subtracting the mean relevance weights over all the 50 TIMIT phonemes.

The top row shows the weights for vowels under clean condition. It can be observed that almost all the vowels have higher contrast in relevance weight values for the rate frequency in $0 – 12$ Hz rate and $-1$ to $9$ cyc./oct scale. Additionally, most of the back and mid vowels elicit higher contrast in weights for band-pass rate and low-pass scale frequencies. In the low SNR condition, for vowels (second row of Figure 7 with SNR = 0 dB), the relevance characteristics are much more intact compared to the acoustic FB layer relevance weights, with more contrast in lower rate regions. In case of consonants (third and fourth row of Figure 7), for the clean case, the plosive /t/ show similar trend as mid vowels while the fricative /sh/ show a low-pass rate + high-pass scale contrast profile. Additionally, most of the consonants have high contrast towards low-pass rate + high-pass scale and band-pass rate + low-pass scale region. On the other hand, the noisy consonants (SNR 0 dB) show low-pass rate profile scattered over different scale values.

V. Experiments and Results

The speech recognition system is trained using PyTorch toolkit \cite{paszke2019pytorch} while the Kaldi toolkit \cite{povey2011kaldi} is used for decoding and language modeling. The models are discriminatively trained using the training data with cross entropy loss and Adam optimizer \cite{kingma2014adam}. A hidden Markov model - Gaussian mixture model (HMM-GMM) system is used to generate the senone alignments for training the CNN-DNN based model. The ASR results are reported with a tri-gram language model and the best language model weight is obtained from the development set. The notation [A,M] refers to the model of learning acoustic and modulation filterbanks without relevance, [A-R,M] refers to the model that involves acoustic FB with relevance along with modulation FB without relevance, [A, M-R] refers to learning acoustic FB (with no relevance weighting), followed by modulation filter learning with relevance weighting, and [A-R,M-R] refers to the model with learning acoustic and modulation FB and having relevance weighting in both layers. The modulation filters are learnt in all baseline features as well as the first 2-D CNN layer.

For each dataset, we compare the ASR performance of the proposed approach with traditional mel filterbank energy (MFB) features, power normalized filterbank energy (PFB) features \cite{schwandt2009power}, RASTA features that perform modulation filtering (RAS) \cite{kawahara2007rasta}, and mean Hilbert envelope (MHE) features \cite{matsuoka1999hilbert}. All the baseline features are processed with cepstral mean and variance normalization (CMVN) on a 1 sec. running window. The baseline MFB features are directly fed to the 2-D modulation filtering layer (without the acoustic FB layer). The other baseline features like PFB, RAS and MHE also generate spectrogram like time-frequency representations which are used similar to the MFB features. For all these features, no relevance weighting is performed. The modulation filtering layer (M) is part of the baseline system and is present with all the other features like PFB, RAS, MHE (without explicit mention in all cases). An additional experiment, where relevance weighting is applied on the baseline MFB features (denoted as MFB-R) is also performed. For ASR experiments on the proposed model, we use a non-parametric approach in modulation filter learning. The non-parametric approach to modulation filtering involves learning 2-D kernels of the CNN layer that operates on the output of the acoustic FB layer. Empirically, the non-parametric modulation filters had a
Fig. 9. The modulation relevance weights (after removing the mean weights) plotted for each phoneme: vowel phonemes in top two rows for clean and SNR 0 dB condition and consonants in the last two rows for clean and SNR 0 dB condition respectively. The size of the bubble is proportional to the magnitude of the relevance weight.

A. Aurora-4 ASR

Aurora-4 database consists of continuous read speech recordings of 5000 words corpus, recorded under clean and noisy conditions (street, train, car, babble, restaurant, and airport) at 10 – 20 dB SNR. The training data has 7138 multi condition recordings (84 speakers) with total 15 hours of training data. The validation data has 1206 recordings for multi condition setup. The test data has 330 recordings (8 speakers) for each of the 14 clean and noise conditions. The test data are classified into group Aur-A - clean data, Aur-B - noisy data, Aur-C - clean data with channel distortion, and Aur-D - noisy data with channel distortion.

The ASR performance on the Aurora-4 dataset is shown in Table I for each of the 14 test conditions. As seen in the results, most of the noise robust front-ends do not improve over the baseline mel filterbank (MFB) performance. The proposed representation learning (two-stage relevance weighting) provides considerable improvements in ASR performance over the baseline system with average relative improvements of 11% over the baseline MFB features. Furthermore, the improvements in ASR performance are consistently seen across all the noisy test conditions.

1) Statistical Significance: In order to compare how one system performs relative to the other in statistical sense, we use the bootstrap estimate for confidence interval [48]. This method computes a bootstrapping of word error rate (WER) values to extract the 95% confidence interval (CI), and also gives a probability of improvement (POI) for the system-in-test (system with the proposed representation learning) over the reference system (baseline system with MFB features). Table II shows the analysis for various test conditions in the Aurora-4 multi-condition training. The POI of the proposed system (A-R,M-R) system over the MFB is quite high for all the test conditions, with average POI being 94%.

B. CHiME-3 ASR

The CHiME-3 corpus for ASR contains multi-microphone tablet device recordings from everyday environments, released...
The results for the CHiME-3 dataset are reported in Table IV. The approach of acoustic FB learning with relevance weighting alone (A-R) improves over the baseline system learned acoustic representations and modulation representations (A-M-R) provides significant improvements over baseline features. On the average, the proposed approach provides relative improvements of 18.5% over MFB features in real development and evaluation utterances. The results for the CHiME-3 dataset are reported in Table IV. The approach of acoustic FB learning with relevance weighting alone (A-R) improves over the baseline system learned acoustic representations and modulation representations (A-M-R) provides significant improvements over baseline features. On the average, the proposed approach provides relative improvements of 10% over MFB features in the eval set. The detailed results on different noises in CHiME-3 are reported in Table IV. For most of the noise conditions in CHiME-3 in simulated and real environments, the proposed approach provides consistent improvements over the baseline features.

### C. VOiCES ASR

The Voices Obscured in Complex Environmental Settings (VOiCES) corpus is a creative commons speech dataset [1]. The training data set of 80 hours has 22,741 utterances sampled at 16kHz from 202 speakers, with each utterance having 12 – 15s segments of read speech from the Librispeech corpus. We performed a 1-fold reverberation and noise augmentation of the data using Kaldi [14]. The ASR development set consists of 20 hours of distant recordings from the 200 VOiCES dev speakers. It contains recordings from 6 microphones. The evaluation set consists of 20 hours of distant recordings from the 100 VOiCES eval speakers and contains recordings from 10 microphones from an unseen room. The ASR performance of VOiCES dataset with baseline MFB features and our proposed approach of 2-stage relevance weighting is reported in Figure 10. These results suggest that the proposed model is also scalable to relatively larger ASR tasks with large vocabulary where consistent improvements are obtained with the proposed approach in addition to the interpretability of the representations learned.

### VI. DISCUSSION

#### A. Effect of relevance weighting on different stages

We compare the ASR performance of the proposed approach of 2-stage relevance weighting (A-R,M-R) with the learned acoustic FB representation (A) without any relevance weighting, relevance weighting on fixed mel filterbank features (MFB-R), acoustic FB relevance weighting without modulation FB relevance weighting (A-R), and modulation relevance weighting alone on learned time-frequency representation (A,M-R). We also report performance with handcrafted filterbanks at both the stages, denoted as [MFB-R, G-R]. The hand-crafted modulation filters (G) were chosen as 2-D cosine-modulated Gaussian filters with pre-determined ratescale center frequencies. Based on prior studies, we use more filters in the band-pass rate and low pass scale regions.

The results are reported in Table V averaged for 4 test conditions of Aurora-4 dataset. Since the modulation filtering layer (M) is part of the baseline system and is present with all being used as part of VOiCES Challenge [51].
the rest of the architecture is kept the same as shown in Fig. 1.

The ASR system with sincFB and 2-stage relevance weighting is also trained. In addition, we also compare with acoustic FB learning in a non-parametric (ANP) manner (learning the 1-D CNN kernels directly from raw input without using a cosine modulated Gaussian function) [3], [5], [7].

The ASR performance is reported in Table VII for mel filterbank features (MFB), our proposed cosine modulated Gaussian filterbank without relevance weighting (R) and the sinc filterbank from [14] (Sinc). For the experiments without relevance weighting, it can be observed that the parametric sinc filterbank performs similar to our acoustic filterbank, and both perform similar to mel filterbank. The relevance weighting over sinc FB (Sinc-R,M-R) improves over the baseline with average relative improvement of around 6% over MFB, while the proposed [A-R,M-R] representation improves over the sinc FB approach. The proposed parametric approach to acoustic FB learning also improves over the non-parametric (ANP) approach.

In addition, to compare the relevance weighting approach with the self-attention approach, we train an ASR model with the acoustic FB relevance sub-network replaced with self-attention module (with self-attention weighting on sub-bands) for the acoustic filterbank layer. From the ASR performance for this system (A-SelfAttn,M), it can be observed that the relevance weighting proposed in this work is superior to channel weighting based on self-attention.

D. Unsupervised vs. Supervised representation learning

In our proposed approach, the parametric kernels of the acoustic FB layer can be initialized in different ways: (i) initialization using unsupervised training of CVAE [9], (ii) unsupervised initialization + supervised fine tuning in ASR, and (iii) random initialization + supervised fine tuning. Table VIII shows the effects of acoustic FB initialization on ASR. All the features are trained with the proposed relevance weighting based model. For the random initialization, we sample the center frequencies uniformly at random or use a sigmoidal mapping function on the uniform random variable. It can be observed that unsupervised initialization alone of acoustic FB parameters (and no fine tuning) does not improve over baseline. The random initialization of acoustic FB followed by supervised fine-tuning for ASR gives considerable improvement in ASR performance. The random initialization
TABLE VIII
UNSUPERVISED LEARNING VS. SUPERVISED LEARNING OF ACOUSTIC FILTERBANK WITH [A-R,M-R] CONFIGURATION ON AURORA-4 DATASET.

| Type of acoustic FB learning | ASR (WER in %) |
|-----------------------------|----------------|
| Random Initialization on uniform scale + No fine tuning | 11.9 |
| Random Initialization on sigmoidal frequency scale + No fine tuning | 11.2 |
| Unsupervised Initialization (& no fine tuning) | 10.9 |
| Unsupervised Initialization + supervised fine tuning | 9.6 |
| Random Initialization on sigmoidal scale + supervised fine tuning | 9.9 |

TABLE IX
EFFECT OF CONTEXT LENGTH OF THE INPUT PATCH (VALUE OF $t$) ON AURORA-4 ASR PERFORMANCE WITH THE [A-R,M-R] APPROACH.

| Context length (value of $t$) | ASR (WER in %) |
|-----------------------------|----------------|
| 21                          | 10.2           |
| 51                          | 10.1           |
| 81                          | 10.0           |
| 101                         | 9.6            |
| 131                         | 9.6            |

E. Choice of hyper-parameters

We experiment with various choices of hyper-parameters in acoustic FB learning. The effect of context length of the input patch ($t$) is analyzed through ASR performance with the proposed [A-R, M-R] approach. The Aurora-4 dataset is used with different context length of $t = 21, 51, 81, 101$ and $131$. From the results reported in Table IX, it can be observed that the performance improves with increasing the context length, with the best performance for $t = 101$ and $t = 131$.

We also observe the effect of acoustic filter length $k$. While $k = 8$ms yields a frequency resolution of 125Hz, a 4ms long kernel has a frequency resolution of 250Hz and a 16ms long kernel has a frequency resolution of 62.5Hz. The baseline features like mel filter bank use windowing in the frequency domain with mel-spaced filters. The filters in the lower frequency range in the mel-scale have higher resolution (around 100 Hz). From Table IX, it can be observed that while the shorter filter length degrades the ASR performance, the increased filter length beyond 8ms does not improve the ASR performance.

F. Urban Sound Classification

The spectro-temporal characteristics of the different types of audio signals are different, and hence, the learned time-frequency representation should capture these distinctive properties for efficient sound classification. The proposed two stage approach of representation learning is explored for urban sound classification task. The same architecture used for speech (shown in Figure 1) is used for audio representation learning. The input to the network is a short audio snippet and the network is trained for classifying 10 urban sound classes. Following the acoustic FB layer and the modulation filtering layer (with the two relevance weighting sub-networks), the model consists of a CNN-LSTM for the USC task (the LSTM backend provided an improved performance for the USC task but not for the ASR task).

1) Dataset: The USC system is trained using PyTorch [43] using UrbanSound8K dataset [53]. It contains 8732 sound clips sampled at 44.1kHz, with duration up to 4s divided into 10 sound classes: air conditioner (AI), car horn (CA), children playing (CH), dog bark (DO), drilling (DR), engine idling (EN), gun shot (GU), jackhammer (JA), siren (SI) and street music (ST). The best trained model is chosen through cross-validation loss. In our work, we use 9 folds for training purpose, and the results are reported with average of 10-fold cross validation.

Fig. 11 shows the center frequency ($\mu_t$ values sorted in ascending order) of the acoustic filters obtained for the USC task. A comparison with the mel filter center frequencies as well as learnt center frequency from Aurora-4 speech data is also provided for reference. The center frequency of learned filters in audio data deviate from the mel counterparts. In particular, the learned representations have more emphasis on higher frequencies compared to the mel spectrogram.

Table X reports the average USC performance for baseline system and the proposed two-stage approach of representation learning. As seen in the results, the learnt acoustic FB features (A) alone (without any relevance weighting) performs considerably better than the fixed MFB features, with an absolute

TABLE X
EFFECT OF DIFFERENT FILTER LENGTH ($k$) IN ACOUSTIC FB LAYER ON ASR PERFORMANCE WITH AURORA-4 DATASET.

| Filter length (value of $k$) | ASR (WER in %) |
|-----------------------------|----------------|
| 64 (4ms)                    | 10.6           |
| 128 (8ms)                   | 9.6            |
| 256 (16ms)                  | 9.7            |
The acoustic FB relevance weights for the audio signals are analyzed in Fig. 12. It can be observed that most of the sounds exhibit higher relevance weight for low to mid acoustic frequencies, with drilling and jackhammer sounds having significant weight values till the end of the spectral range. The air conditioner and engine idling have low frequency sounds with peak primarily in between 10 – 200Hz. The car horn, siren and street music sounds exhibit multiple frequencies and hence, have higher value for relevance weights till around 4kHz. The gun-shot sound weight profile exhibits an exclusive peak at around 550Hz.

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**G. Contributions Beyond Prior Works**

The self-attention approach [54] applies a fixed neural layer on inputs (typically hidden layer activations indexed by time) to generate a single scalar value. A softmax operation applied on the scalar values over time provides the attention weights. The attention weights are used to generate a linear combination of the embeddings. In the proposed work, while a softmax operation on scalar relevance weight values are performed, we do not perform any linear combination of the inputs. Thus, the scalar values act as a relevance weights (gain) that modulate the information flow to the subsequent layers. A higher value of the weight signifies more relevance to the corresponding input stream (sub-band in acoustic FB layer or modulation filter in the modulation FB layer). In addition, self-attention in LSTM networks are typically performed at the end of the encoding layers (closer to the target layer) or as multiple modules of self-attention in transformer networks [24] which carry all the way up to the target layers. In the proposed framework, the relevance weighting is only performed in the initial layers which are closer to the input representations. Hence, the relevance weights offer interpretability in terms of speech/audio characteristics.

The gated neural network approach [23] explored multiple parallel “expert” networks followed by a gating network which performs a convex combination of the outputs from the networks. Again, similar to self-attention, the model only propagates the combined output. The ASSERT network [55] for spoof detection proposes an attention filtering layer. This approach operates on speech spectrograms of the entire utterance (typically few seconds) and generates an attentional heat-map using a deep convolutional neural network with a U-net model containing multiple levels of dialation, downsampling and upsampling layers along with skip connections. The attentional heat-map is then element wise multiplied on the input utterance spectrogram and added with input spectrogram. The entire model is trained for spoof detection task. In the proposed approach, the model does not generate a heat-map on all components. It rather provides a scalar relevance weight for each sub-band (acoustic FB layer) or for each modulation filter (modulation FB layer). In addition, the proposed model does not add the weighted input again with the input but rather propagates the weighted feature stream directly to the subsequent layers. Further, the authors in ASSERT use the attention filtering only on the input log-magnitude spectrogram. The ASSERT attention filtering will be more cumbersome than the proposed approach when incorporated in modulation filtering layers as the attentional heat-map needed would be 3-D in nature.
A. Key Contributions

The key contributions of the work can be summarized as follows:

- Posing the representation learning problem in an interpretable filterbank learning framework using relevance weighting mechanism from raw waveform.
- Using a two-step process for learning representations: first step to obtain time-frequency (spectrogram) representation from raw waveform; second step to perform modulation filtering on first step output. Both steps have separate relevance weighting sub-networks, which are differentiable and can be easily integrated in the backpropagation learning.
- Implementing the acoustic filterbank in the first convolutional layer of the proposed model using a parametric cosine-modulated Gaussian filter bank whose parameters are learned. A relevance sub-network provides relevance weights to acoustic FB.
- The second convolutional layer performs modulation filtering over the first layer output. Another relevance sub-network provides relevance weights to the modulation feature maps.
- ASR experiments on a variety of speech datasets containing noise and reverberation showing the benefits of the proposed approach.
- Analysis of the relevance weights reveal that the weights capture underlying phonetic content in speech.
- The proposed 2-stage framework is extended to urban sound classification task where it shows improved performance. The weight analysis reveals that distinct audio characteristics are captured by the relevance weights.

B. Limitations

Some limitations of the proposed work include,

- The proposed approach is empirical. The model is proposed and analyzed based on performance metrics.
- The total number of parameters in the mel-scale baseline is around 27.92M while in the proposed approach the number of trainable parameters is 27.98M. In terms of total number of parameters involved, the proposed approach only increases the number of parameters by 0.2%. In terms of computational time, we performed an experiment with 100 test files from the Aurora-4 corpus and measured the computation time for forward pass through the model for the baseline system as well as the proposed relevance weighted model. The computation time for the proposed model increased by 20% (171sec. of computational time for the proposed method versus 136sec. for the baseline mel-spec system).

C. Future Work

The relevance weighting should also incorporate some level of feedback if the proposed model is to imitate biology in true sense. In addition, other gross statistics of the signal maybe potentially useful in deriving the relevance weights. Furthermore, extending the approach to representation learning for other machine learning tasks like speaker recognition and language modeling are part of future considerations.

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The implementation of the proposed approach is available at https://github.com/PurviAgrawal/Interpretable_rawWaveform_relevanceWeighted
