Family Non-universal $U(1)'$ Gauge Symmetries and $b \to s$ Transitions

Vernon Barger,$^1$ Lisa Everett,$^1$ Jing Jiang,$^1$ Paul Langacker,$^2$ Tao Liu,$^3$ and Carlos E.M. Wagner$^{3,4,5}$

$^1$Department of Physics, University of Wisconsin, Madison, WI 53706
$^2$School of Natural Science, Institute for Advanced Study, Einstein Drive, Princeton, NJ 08540
$^3$Enrico Fermi Institute, University of Chicago, 5640 S. Ellis Ave., Chicago, IL 60637
$^4$Kaei Institute for Cosmological Physics, University of Chicago, 5640 S. Ellis Ave., Chicago, IL 60637
$^5$HEP Division, Argonne National Laboratory, 9700 Cass Ave., Argonne, IL 60439

We present a correlated analysis for the $\Delta B = 1,2$ processes which occur via $b \to s$ transitions within models with a family non-universal $U(1)'$. We take a model-independent approach, and only require family universal charges for the first and second generations and small fermion mixing angles. The results of our analysis show that within this class of models, the anomalies in $B_s - \bar{B}_s$ mixing and the time-dependent CP asymmetries of the penguin-dominated $B_d \to (\pi, \phi, \eta', \rho, \omega, f_0)K_S$ decays can be accommodated.

During the past several decades, great progress has been made in understanding CP-violating phenomena in the meson systems. With the advent of the B factories, it has been established that the observed CP violation in the $B_d$ and $K$ systems can be accommodated within the Standard Model (SM), sourced by the single phase of the Cabibbo-Kobayashi-Maskawa flavor mixing matrix $|\theta_{13}|$. Despite the success of the SM picture of CP violation, it is known that additional sources of CP violation are needed in nature, for example to explain the origin of the baryon asymmetry of the universe. Such additional phases, which arise in many models of new physics (NP) at the TeV scale, can result in competitive contributions to CP violation for processes in which the SM contribution enters at loop level, such as in $b \to s$ transitions. Indeed, recent measurements of a number of such observables exhibit discrepancies with SM predictions at the level of a few standard deviations, which may reveal the tantalizing possibility of physics beyond the SM.

The first relevant observable of this type is the $B_s - \bar{B}_s$ mixing phase, which is parametrized by the off-diagonal mixing matrix element

$$M_{12} = (M_{12}^B)_{SM} C_{B_s} e^{2i\phi_{NP}}.$$  

In the SM, the modulus $C_{B_s}$ and phase $\phi_{NP}$ are equal to one and zero, respectively. A recent analysis $^2$ finds that $\phi_{NP}$ deviates by more than $3\sigma$ from zero (see Table I), by combining all the available experimental information on $B_s$ mixing, including the new tagged analysis of $B_s \to \psi K_S$ by CDF $^3$ and DØ $^4$. The discrepancy disfavors NP scenarios which obey minimal flavor violation (e.g., see $^5$), i.e., with $\phi_{NP} \approx 0$, and instead suggests NP which exhibits flavor violation in the $b \to s$ transitions.

Another set of emblematic examples is the set of time-dependent CP asymmetries in the charmless hadronic $b \to s\bar{q}q$ ($q = u,d,c,s$) decays. The SM predicts that many decays in this class, including $B_d \to \psi K_S$ and $B_d \to (\phi, \eta', \rho, \omega, f_0)K_S$, obey the relations (e.g., see $^6$)

$$-\eta_{fCP} S_{fCP} \simeq \sin 2\beta, \quad C_{fCP} \simeq 0,$$

in which $\eta_{fCP} = \pm 1$ is the CP eigenvalue for the final state $fCP$ and $\beta \equiv \arg[-(V_{td}V_{tb}^*)/(V_{td}V_{tb}^*)]$. However, the central values of $\sin 2\beta$ directly measured from the penguin-dominated modes are systematically below the SM prediction and the results obtained from measuring the charmless $B_d \to \psi K_S$ mode (see Table I). Given that $b \to s\bar{c}c$ is dominated by the SM tree-level amplitude, $\Delta S_{fCP} = -\eta_{fCP} S_{fCP} + \eta_{K_S} S_{\psi K_S} \neq 0$ may imply interesting NP in the penguin-dominated decay modes.

To account for these possible discrepancies in the $b \to s$ transitions, a number of NP scenarios have been studied (e.g., see $^7$). In this letter, we will study these anomalies within the NP scenarios with a family non-universal gauged $U(1)'$ symmetry (see also $^8$). Additional $U(1)'$ gauge symmetries naturally exist in many well-motivated extensions of the SM (e.g., see $^9$). The associated gauge charges for the SM fermions $\tilde{e}_{ij}^{s\bar{q}q}$ can be diagonalized

| Observable | 1$\sigma$ C.L. | 2$\sigma$ C.L. |
|----------------|----------------|----------------|
| $\phi_{NP}$ (S1) | $-19.9 \pm 5.6$ | $[-30.45,-9.29]$ |
| $\phi_{NP}$ (S2) | $-68.2 \pm 4.9$ | $[-78.45,-58.2]$ |
| $C_{B_s}$ | $1.07 \pm 0.29$ | $[0.62,1.93]$ |

TABLE I: The fit results for the $B_s - \bar{B}_s$ mixing parameters $^2$. The two solutions for $\phi_{NP}$, denoted as “S1” and “S2”, result from measurement ambiguities; see $^2$ for details.

| $fCP$ | $-\eta_{fCP} S_{fCP}$ ($1\sigma$ C.L.) | $C_{fCP}$ ($1\sigma$ C.L.) |
|--------|---------------------------------|----------------|
| $\psi K_S$ | $+0.672 \pm 0.024$ | $+0.005 \pm 0.019$ |
| $\phi K_S$ | $+0.44_{-0.17}^{+0.17}$ | $-0.23 \pm 0.15$ |
| $\eta' K_S$ | $+0.59 \pm 0.07$ | $-0.05 \pm 0.05$ |
| $\pi K_S$ | $+0.57 \pm 0.17$ | $+0.01 \pm 0.10$ |
| $\rho K_S$ | $+0.63_{-0.21}^{+0.17}$ | $-0.01 \pm 0.20$ |
| $\omega K_S$ | $+0.45 \pm 0.24$ | $-0.32 \pm 0.17$ |
| $f_0 K_S$ | $+0.62_{-0.13}^{+0.11}$ | $0.10 \pm 0.13$ |

TABLE II: World averages of the experimental results for the CP asymmetries in $B_d$ decays via $b \to s\bar{q}q$ transitions $^6$. 

arXiv:0902.4507v2 [hep-ph] 16 May 2009
with a proper choice of gauge basis. Here $\psi$ represents the quarks and leptons, and $i,j$ are family indices. For $U(1)'$ models in which the gauge charges are family non-universal, the $Z'$ couplings are affected by fermion mixings and are not diagonal in the mass basis. Non-trivial flavor-changing neutral current (FCNC) effects mediated by the $Z'$ therefore are induced. The formalism for such effects is systematically developed in [10] [11]. Explicitly, the strong limits from $K - \bar{K}$ mixing and $\mu - e$ conversion exclude significantly non-universal couplings for the first two families for a TeV-scale $Z'$, suggesting an approximate coupling structure in the basis of the mass eigenstates of $\psi_{L,R}^{}$:

$$B^{\psi_{L,R}} = \frac{g_2 M_Z}{g_1 M_{Z'}} V_{\psi_{L,R}}^{\psi_{L,R}} V_{\psi_{L,R}}^{\dagger} \equiv \begin{pmatrix} B_{11}^{\psi_{L,R}} & 0 & B_{13}^{\psi_{L,R}} \\ 0 & B_{22}^{\psi_{L,R}} & 2B_{23}^{\psi_{L,R}} \\ B_{13}^{\dagger \psi_{L,R}} & B_{23}^{\dagger \psi_{L,R}} & B_{33}^{\dagger \psi_{L,R}} \end{pmatrix}, \quad (3)$$

in which $V_{\psi_{L,R}}^{\psi_{L,R}}$ are the unitary matrices that diagonalize the fermion mass matrices. $B^{\psi_{L,R}}$ differs from the definitions in [10] by the factor $g_2 M_Z / g_1 M_{Z'}$ ($g_1, g_2$ denote the perturbative $Z$ and $Z'$ couplings). Hermiticity dictates that there are only two phases, associated with $B^{\psi_{L,R}}_{13}$ and $B^{\psi_{L,R}}_{23}$, respectively. Such a structure can be obtained by simply assuming $\epsilon_{13}^{\psi_{L,R}} = \epsilon_{23}^{\psi_{L,R}}$ and small fermion mixing angles [11]. It demonstrates that non-universal $Z'$ effects can contribute to $\Delta B = 1, 2$ processes via $b \to s$ transitions. In this letter, we will neglect the effects of $B^{\psi_{L,R}}_{13}$, and assume no $Z - Z'$ mixing and no $Z'$-mediated mixing between ordinary and exotic fermions which may also result in nontrivial FCNC effects (e.g., see [9]).

The $Z'$ contributions to FCNC are at tree level, and hence they may be competitive even for small couplings. Depending on the details of the $U(1)'$ model, such $Z'$ effects can result both in new FC operators and modified Wilson coefficients to the effective SM operators in the operator product expansion. The details of this formalism for the $b \to s$ transitions will be presented in [11]. Here we summarize the necessary elements. For $B_s - B_s$ mixing and $b \to s \bar{q}q$, the modifications to the effective Hamiltonians are respectively given by

$$H_{eff}^{Z'}(B_s - \bar{B}_s) = \frac{-G_F}{\sqrt{2}} (\Delta C_{1B_s} Q_1^{B_s} + 2\Delta \tilde{C}_{3B_s} Q_3^{B_s} + \Delta C_{1B_s}^* Q_1^{B_s} ) + h.c. \quad (4)$$

$$H_{eff}^{Z'}(b \to s \bar{q}q) = \frac{-G_F}{\sqrt{2}} V_{tb} V_{ts}^* (\Delta C_{3Q^3} + \Delta C_{5Q^5} + \Delta C_{7Q^7} + \Delta C_{9Q^9} + \Delta \tilde{C}_{5Q^5} + \Delta \tilde{C}_{7Q^7} + \Delta \tilde{C}_{9Q^9}) + h.c., \quad (5)$$

in which the $Q$s represent the SM operators [12], and the $\tilde{C}$s are new operators introduced by the NP $(\tilde{Q}_3^{B_s} = (s\bar{b})_{U+A}(s\bar{b})_{V-A})$; the $Q, \tilde{Q}$ with the same superscript and subscript are related by chirality-flipping). For simplicity, in this letter we will work in the limit that $B_{bs}^L = B_{bs}^R$ for the quark sector, in which the nontrivial $Z'$ corrections to the Wilson coefficients are

$$\Delta C_{1B_s} = \Delta \tilde{C}_{1B_s} = \Delta C_{3B_s} = -(B_{bs}^L)^2,$$

$$\Delta C_3 = \Delta \tilde{C}_5 = -2 V_{tb} V_{ts}^* B_{bs}^L B_{dd}^L,$$

$$\Delta \tilde{C}_3 = \Delta C_5 = -2 V_{tb} V_{ts}^* B_{bs}^R (B_{uu}^R + 2B_{dd}^R),$$

$$\Delta C_7 = \Delta \tilde{C}_9 = -\frac{4}{3} V_{tb} V_{ts}^* B_{bs}^R (B_{uu}^R - B_{dd}^R). \quad (5)$$

Though $Z'$-mediated effects can occur in both the QCD and electroweak (EW) penguins, we assume that they are mainly manifest in the EW ones, i.e., $|\Delta C_{3,5} | \ll |\Delta C_{7,9} |$. In this limit, there are three independent parameters: the modulus of $B_{bs}^L$, its phase $\phi_{bs}^L$, and the real $B_{dd}^R(= -B_{uu}^R/2)$.

In contrast to the studies in [8], which are based on mode-by-mode analyses, we will take a correlated analysis for the $\Delta B = 1, 2$ processes which occur via $b \to s$ transitions (for general discussions on the relevant calculations, see e.g. [12]). We focus first on $B_s - \bar{B}_s$ mixing. With the renormalization scale chosen as the $b$-quark mass, 4.2 GeV, the NP probes $C_{B_s}$ and $\phi_{B_s}^N$ are given by

$$C_{\phi_{B_s}^N} = 1 - 3.59 	imes 10^5 (\Delta C_{1B_s} + \Delta \tilde{C}_{1B_s}) + 2.04 	imes 10^6 \Delta \tilde{C}_{3B_s} + 2 \times 10^6 \Delta \tilde{C}_{9B_s} \quad (6)$$

which involves two of the three free parameters: $|B_{bs}^L|$ and $\phi_{bs}^L$. In Fig. [1] their experimental constraints from $B_s - \bar{B}_s$ mixing are illustrated. There are two separate shaded regions, corresponding to the two $\phi_{B_s}^N$ solutions (see Table I). For each region, the various colors of points specify different confidence levels (C.L.) of the relevant $C_{B_s}$ and $\phi_{B_s}^N$ values. To explain the discrepancy of the

![FIG. 1: Constraints on the $|B_{bs}^L|$ and $\phi_{bs}^L$ are presented. Random values for $C_{B_s}$ and $\phi_{B_s}^N$ from the physical regions (see Table I) are mapped to the $|B_{bs}^L|$-$\phi_{bs}^L$ plane using Eq. (6). For the numerical work in this letter, a 25% uncertainty (a typical value from non-perturbative effects) is universally assumed for the coefficients in the NP correction terms.](image-url)
observed $B_s - \bar{B}_s$ mixing from the SM prediction, $|B_{bs}^L|$ is required to be $\sim 10^{-3}$. This follows from Eq. (6) and the fact that $C_{B_s}$ does not deviate from its SM prediction significantly. The smallness of $|B_{bs}^L|$ can help satisfy the experimental constraints of the branching ratio $Br(B_s \rightarrow \mu^+\mu^-)$ easily [11], and is generically consistent with our assumption of small fermion mixing angles, since $B_{bs}^{L_r}$ is proportional to these mixing angles [11].

A process of particular interest is the $B_d \rightarrow \pi K_S$ decay, which has received considerable interest in literatures (see e.g. [13]-[17]). In [13] it is pointed out that a deviation of $S_{\pi K_S}$ from its SM prediction can be understood as a modification of the ratio $q e^{i\phi} = \frac{P}{T + C}$, in which $T$, $C$ and $P$ denote the color-allowed tree, color-suppressed tree, and EW penguin contributions in the decay amplitude, respectively. The non-universal $Z'$ modifies $q e^{i\phi}$ through

$$q e^{i\phi} = 0.76(1 + 158.1\Delta C_7 - 102.4\Delta C_9).$$

The constraints on $q e^{i\phi}$ from $\chi^2$ fit of the $B \rightarrow \pi K$ (and $B \rightarrow \pi \pi$) data have been obtained in [14]. In Fig. 2 we illustrate how $B_{dd}^R$ is constrained through $q e^{i\phi}$, using the parameter values of $|B_{bs}^L|$ and $\phi_{bs}^L$ obtained in Fig. 1 and Eq. (7). There are two distribution regions specified by different colors in this figure, again due to the two $\phi_{bs}^{NP}$ solutions. According to Eq. (7), their right-up branches are related to positive $B_{dd}^R$ values while their left-bottom ones are related to negative $B_{dd}^R$ values.

To obtain acceptable values in both $B_s - \bar{B}_s$ mixing and $B_d \rightarrow \pi K_S$ decay, the NP contributions to $C_{\psi K_S}$ and $S_{\psi K_S}$ are illustrated in the first five panels of Fig. 3. The colors of the points specify the C.L. that their inverse image points represent in Fig. 1 and Eq. (7). In the last panel the $CP$ asymmetries of the charm $B_d \rightarrow \psi K_S$ decay are presented (with $|V_{ts}| = 3.51 \times 10^{-3}$ used in the SM calculation [18]). For each of these panels, the two boxes specify the $1\sigma$ and $1.7\sigma$ experimentally allowed regions (except in the last one where only the $1\sigma$ box is given), and the dark point denotes the SM limit.
the allowed $|B_{dd}^R|$ values are smaller than 0.08. But, to get a better fit or a better agreement with the experimental data, $|B_{dd}^R| > 10^{-2}$ is typically required. This effect is represented by the dark points in Fig. 4 which correspond to the fitted $C_{(\phi,\rho,\omega,\eta)}S_{(\phi,\rho,\omega,\eta)}$ with a higher standard. This effect can also be seen by requiring a smaller C.L. for the $B_{dd}$ parameter region for $B \to \pi K$ and $B \to \pi \pi$, which will be shown in details in [11]. The favored parameter region for $|B_{dd}^R|$ is consistent with the assumption of trivial $Z'$ effects in QCD penguins and small fermion mixings which requires $|B_{dd}^R| < |B_{dd}^L| \ll |B_{dd}^R|$. Because the value of $|B_{dd}^R|$ is favored to be $\sim 10^{-3}$, this relation can be easily accommodated. In addition this parameter region is of interest for collider detection. Given $(Va_d \tilde{e}_d \bar{V}_{da})_{11} \sim \mathcal{O}(1)$ it implies $g_2 \mathcal{M}_Z \sim 10 - 100$, a range approachable at the LHC for $g_2 \lesssim g_1$ (e.g., see [9]). This fact is also important for the effective Hamiltonian in Eq. (4) where the renormalization group running effect between the $Z'$ mass scale and the EW scale is neglected, which is justified only for a low scale $Z'$ boson.

Our results have been obtained in the limit of $B_{bs}^R = B_{bs}^L$. However, it is straightforward to extend the analysis to other limits, e.g., $\tilde{e}_V^L (\tilde{e}_V^R) \propto I$ while $\tilde{e}_V^L (\tilde{e}_V^R)$ is only constrained by $\tilde{e}_V^L (\tilde{e}_V^R) = \tilde{e}_V^R (\tilde{e}_V^L)$, or to generalize to the case where both of them are only constrained by this relation. Actually, similar results are found. We will present them elsewhere [11].

In conclusion, we have presented a correlated analysis for the $\Delta B = 1, 2$ processes which occur via $b \to s$ transitions within NP models with a family non-universal $U(1)'$. In our model-independent approach, the main assumptions are generation-independent charges for the first two families and small fermion mixing angles. We find that within this class of family non-universal $U(1)'$ models, the anomalies in $B_s - B_s$ mixing and the time-dependent CP asymmetries of the penguin-dominated $B_d \to (\pi, \phi, \eta', \rho, \omega, f_0) K_S$ can be accommodated.

Acknowledgements

We thank Cheng-Wei Chiang and Jonathan L. Rosner for useful discussions. Work at ANL is supported in part by the U.S. Department of Energy (DOE), Div. of HEP, Contract DE-AC02-06CH11357. Work at ESI is supported in part by the DOE through Grant No. DE-FG02-90ER40560. Work at the U. Wisconsin, Madison is supported by the DOE through Grant No. DE-FG02-95ER40896 and the Wisconsin Alumni Research Foundation. T.L. is also supported by the Fermi-McCombick Fellowship. The work of P.L. is supported by the IBM Einstein Fellowship and by NSF grant PHY-0503584.

[1] N. Cabibbo, Phys. Rev. Lett. 10, 531 (1963); M. Kobayashi and T. Maskawa, Prog. Theor. Phys. 49, 652 (1973).
[2] M. Bona et al. [UTfit Collaboration], arXiv:0803.0659 [hep-ph].
[3] T. Aaltonen et al. [CDF Collaboration], Phys. Rev. Lett. 100, 161802 (2008).
[4] V. M. Abazov et al. [D0 Collaboration], Phys. Rev. Lett. 101, 241801 (2008).
[5] C. Tarantino, Nuovo Cim. 123B, 437 (2008).
[6] E. Barberio et al., arXiv:0808.1297 [hep-ex]; http://www.slac.stanford.edu/xorg/flag/.
[7] B. Dutta and Y. Mimura, Phys. Rev. D 78, 071702 (2008); M. Blanke, A. Buras, S. Recksiegel and C. Tarantino, arXiv:0805.4393 [hep-ph]; A. Soni, A. Alok, A. Giri, R. Mohanta and S. Nandi, arXiv:0807.1971 [hep-ph]; M. Blanke, A. Buras, B. Duling, S. Gori and A. Weiler, JHEP 0903 (2009) 001.
[8] V. Barger, C. W. Chiang, P. Langacker and H. S. Lee, Phys. Lett. B 580, 186 (2004); Phys. Lett. B 598, 218 (2004); V. Barger, C. W. Chiang, J. Jiang and P. Langacker, Phys. Lett. B 596, 229 (2004); X. G. He and G. Valencia, Phys. Rev. D 74, 013011 (2006); K. Cheung, C. W. Chiang, N. G. Deshpande and J. Jiang, Phys. Lett. B 652, 285 (2007); R. Mohanta and A. K. Giri, arXiv:0812.1842 [hep-ph].
[9] P. Langacker, arXiv:0801.1345 [hep-ph].
[10] P. Langacker and M. Plumacher, Phys. Rev. D 62, 013006 (2000).
[11] V. Barger, L. Everett, J. Jiang, P. Langacker, T. Liu and C. Wagner, in preparation.
[12] G. Buchalla, A. J. Buras and M. E. Lautenbacher, Rev. Mod. Phys. 68, 1125 (1996); A. Ali, G. Kramer and C. D. Lu, Phys. Rev. D 58, 094009 (1998).
[13] A. J. Buras, R. Fleischer, S. Recksiegel and F. Schwab, Phys. Rev. Lett. 92, 101804 (2004); Nucl. Phys. B 697, 133 (2004).
[14] R. Fleischer, S. Jager, D. Pirjol and J. Zupan, Phys. Rev. D 78, 111501 (2008).
[15] M. Gronau and J. Rosner, Phys. Lett. B 666, 467 (2008).
[16] C. W. Chiang, M. Gronau, J. L. Rosner and D. A. Suprun, Phys. Rev. D 70, 034020 (2004); S. Baek, C. W. Chiang and D. London, arXiv:0903.3086 [hep-ph].
[17] M. Ciuchini, E. Franco, G. Martinelli, M. Pierini and L. Silvestrini, Phys. Lett. B 674, 197 (2009).