Abstract We propose a novel scenario of generating lepton asymmetry via annihilation and coannihilation of dark sector particles including t-channel processes. In order to realistically implement this idea, we consider the scotogenic model having three right handed neutrinos and a new scalar doublet, all of which are odd under an in-built $Z_2$ symmetry. The lightest $Z_2$ odd particle, if electromagnetically neutral, can be a dark matter candidate while annihilation and coannihilation between different $Z_2$ odd particles into standard model leptons serve as the source of lepton asymmetry. The light neutrino masses arise at one loop level with $Z_2$ odd fields going inside the loop. We show that experimental data related to light neutrinos, dark matter relic abundance and baryon asymmetry can be simultaneously satisfied in the model for two different cases: one with fermion dark matter and the other with scalar dark matter. In both scenarios, t-channel annihilation as well as coannihilation of $Z_2$ odd particles play a non-trivial role in producing the non-zero CP asymmetry. Both the scenarios remain allowed from DM direct detection while keeping the scale of leptogenesis as low as TeV or less, lower than the one for vanilla leptogenesis scenario in scotogenic model along with the additional advantage of explaining the baryon-dark matter coincidence to some extent. Due to such low scale, the model is testable through rare decay experiments looking for charged lepton flavour violation.

1 Introduction

There have been significant progress in last few decades in gathering evidences suggesting the presence of a mysterious, non-luminous form of matter, known as dark matter (DM) in the present universe, whose amount is approximately five times more than the ordinary luminous or baryonic matter density $\Omega_B \approx 5\%$ [1]. Among different beyond standard model (BSM) proposals for DM, the weakly interacting massive particle (WIMP) paradigm remains the most widely studied scenario where a DM candidate typically with electroweak (EW) scale mass and interaction rate similar to EW interactions can give rise to the correct DM relic abundance, a remarkable coincidence often referred to as the WIMP Miracle. On the other hand, out of equilibrium decay of a heavy particle leading to the generation of baryon asymmetry has been a very well known mechanism for baryogenesis [2,3]. One interesting way to implement such a mechanism is leptogenesis [4] where a net leptonic asymmetry is generated first which gets converted into baryon asymmetry through $B+L$ violating EW sphaleron transitions. The interesting feature of this scenario is that the required lepton asymmetry can be generated within the framework of the seesaw mechanism that explains the origin of tiny neutrino masses [5], another observed phenomena which the SM fails to address.

Although these popular scenarios can explain the phenomena of DM and baryon asymmetry independently, it is nevertheless an interesting observation that DM and baryon abundance are very close to each other, within the same order of magnitudes $\Omega_{DM} \approx 5\Omega_B$. Discarding the possibility of any numerical coincidence, one is left with the task of constructing theories that can relate the origin of these two observed phenomena in a unified manner. There have been several proposals already which mainly fall into two broad categories. In the first one, the usual mechanism for baryogenesis is extended to apply to the dark sector which is also asymmetric [6–9]. The second one is to produce such asymmetries through annihilations [10–12] where one or more particles involved in the annihilations eventually go out of thermal equilibrium in order to generate a net asymmetry. The so-called WIMPy baryogenesis [13–18] belongs to this category, where a dark matter particle freeze out to generate its own relic abundance and then an asymmetry in the baryon sector is produced from DM annihilations.
While there is no evidence yet for seesaw mechanism, recently the so-called scotogenic model [19] as an alternative to canonical seesaw mechanism has been extensively studied, where Majorana light neutrino masses can be generated at one loop level with DM particle in the loop. In the scotogenic model, the required lepton asymmetry can be generated through right handed neutrino decays at a low scale \( M_N \sim 10^{13}\text{TeV} \) at the cost of a strongly hierarchical neutrino Yukawa structure [20,21], but it can not explain the coincidence of baryon asymmetry and DM abundance.

An interesting question raised is whether leptogenesis through (co-)annihilations of \( Z_2 \) odd particles can be realised by lowering the scale of leptogenesis further compared to vanilla leptogenesis in the scotogenic model. Given an answer to this question is the main purpose of this work. We examine how the (co-)annihilations of \( Z_2 \) odd particles can produce the lepton asymmetry while keeping the correct DM abundance, and show that the DM relic abundance is correlated with baryon asymmetry in the scenario. To include all possible annihilations producing lepton asymmetry, we consider the annihilations and coannihilations of all \( Z_2 \) odd particles instead of restricting them to the lightest \( Z_2 \) odd particle which is also the DM candidate. If we consider the neutral component of the \( Z_2 \) odd scalar doublet as DM, then there exists s-channel coannihilation diagrams between DM and right handed neutrinos which can produce a net leptonic asymmetry. While the model satisfies correct DM abundance and lepton asymmetry, the DM sector can be probed at direct detection experiments as well as colliders due to the electroweak gauge interactions of scalar doublet DM. We then consider the fermion DM scenario where the lightest right handed neutrino plays the role of DM. While the annihilation of a pair of the fermionic DM can not produce a net lepton asymmetry in this case, the annihilation of \( Z_2 \) odd scalar doublets can contribute to the generation of lepton asymmetry. Due to the natural absence of typical s-channel diagrams of scalar doublet annihilations leading to lepton asymmetry, here we show how t-channel diagrams (both tree level and one loop level) can play a non-trivial role in creating the required asymmetry.

As far as we know, the contributions of (co-)annihilations of dark sector particles to lepton asymmetry in this minimal model was not considered before. In both the scenarios we address here, the criteria for "on-shell"-ness of loop particles in one loop annihilation diagrams dictate the particle spectrum and hence the nature of dark matter candidate. We show that it is possible to satisfy the requirement of baryon asymmetry, light neutrino mass and DM related constraints in both the scenarios while keeping the scale of leptogenesis as low as 5 TeV, lower than the scale of vanilla leptogenesis in the same model [21,22]. Due to such a low scale, the model has another advantage to predict observable rates of charged lepton flavour violation accessible by the sensitivity of the future experiments.

This paper is arranged as follows. In Sect. 2, we briefly review on the minimal scotogenic model followed by detailed discussion on leptogenesis from annihilation and coannihilations in this model in Sect. 3. We finally conclude in Sect. 4.

2 Minimal scotogenic model

The minimal scotogenic model [19] is the extension of the SM by three copies of right handed singlet neutrinos \( N_i, i \in 1, 2, 3 \) and one scalar field \( \eta \) transforming as a doublet under \( SU(2)_L \). An additional discrete symmetry \( Z_2 \) is incorporated under which these new fields are odd giving rise to the possibility of the lightest \( Z_2 \)-odd particle being a suitable DM candidate. The Lagrangian involving the newly added singlet fermions is

\[
L \supset \frac{1}{2}(M_N)_{ij}N_i N_j + (y_{ij} L_i \bar{\eta} N_j + \text{h.c.}).
\]

(1)

The electroweak symmetry breaking occurs due to the non-zero vacuum expectation value (VEV) acquired by the neutral component of the SM Higgs doublet while the \( Z_2 \)-odd doublet \( \eta \) does not acquire any VEV. After the EWSB these two scalar doublets can be written in the following form in the unitary gauge,

\[
H = \left( \begin{array}{c} 0, \\ \frac{v + h}{\sqrt{2}} \end{array} \right), \quad \eta = \left( \eta^+, \frac{\eta_R + i\eta_I}{\sqrt{2}} \right)^T.
\]

(2)

The scalar potential of the model is

\[
V = \mu_H^2 |H|^2 + \mu_\eta^2 |\eta|^2 + \frac{\lambda_H}{2} |H|^4 + \frac{\lambda_\eta}{2} |\eta|^4 + \lambda_3 |H|^2 |\eta|^2 + \lambda_4 |H^{\dagger} \eta|^2 + \left\{ \frac{\lambda_5}{2} (H^\dagger \eta)^2 + \text{h.c.} \right\}.
\]

(3)

The masses of the physical scalars at tree level can be written as

\[
m_{h^\pm}^2 = \lambda_H v^2,
\]

\[
m_{\eta^\pm}^2 = \mu_\eta^2 + \frac{1}{2} \lambda_3 v^2,
\]

\[
m_{\eta_R}^2 = \mu_\eta^2 + \frac{1}{2} (\lambda_3 + \lambda_4 + \lambda_5) v^2
\]

\[= m_{h^\pm}^2 + \frac{1}{2} (\lambda_4 + \lambda_5) v^2,
\]

\[
m_{\eta_I}^2 = \mu_\eta^2 + \frac{1}{2} (\lambda_3 + \lambda_4 - \lambda_5) v^2
\]

\[= m_{h^\pm}^2 + \frac{1}{2} (\lambda_4 - \lambda_5) v^2.
\]

(4)

Here \( m_h, m_{\eta_R}, \text{and } m_{\eta_I} \) are the masses of the SM like Higgs boson, the CP even and CP odd scalars from the inert doublet, respectively. \( m_{\eta^\pm} \) is the mass of the charged scalar. Without
any loss of generality, we consider $\lambda_5 < 0$, $\lambda_4 + \lambda_5 < 0$ so that the CP even scalar is the lightest $Z_2$ odd particle and hence a stable dark matter candidate.

Denoting the squared physical masses of neutral scalar and pseudo-scalar parts of $\eta$ as $m_{\eta R}^2 = m_{\eta L}^2$ and the mass of the right handed neutrino $N_k$ in the internal line as $M_k$, the one loop neutrino mass can be estimated as [19]

\[
(M_v)_{ij} = \sum_k \frac{\bar{y}_{ik} y_{jk} M_k}{32 \pi^2} \left( \frac{m_{\eta R}^2 - m_{\eta L}^2}{m_{\eta R}^2 - m_{\eta L}^2} \ln \frac{m_{\eta R}^2}{m_{\eta L}^2} - \frac{m_{\eta R}^2 - m_{\eta L}^2}{m_{\eta R}^2 - m_{\eta L}^2} \ln \frac{m_{\eta L}^2}{m_{\eta R}^2} \right) \equiv \sum_k \frac{\bar{y}_{ik} y_{jk} M_k}{32 \pi^2} \left[ L_k (m_{\eta R}^2) - L_k (m_{\eta L}^2) \right],
\]

\[
\Lambda_k = \frac{M_k}{32 \pi^2} \left[ L_k (m_{\eta R}^2) - L_k (m_{\eta L}^2) \right],
\]

where $M_k$ is the mass eigenvalue of the right handed neutrino mass eigenstate $N_k$ in the internal line and the indices $i, j = 1, 2, 3$ run over the three neutrino generations. The function $L_k (m^2)$ is defined as

\[
L_k (m^2) = \frac{m^2}{m^2 - M_k^2} \ln \frac{m^2}{M_k^2}. \tag{6}
\]

From the physical scalar masses given above, we note that $m_{\eta R}^2 - m_{\eta L}^2 = \lambda_5 v^2$. In this model for the neutrino mass to match with experimentally observed limits ($\sim 0.1$ eV), Yukawa couplings of the order $10^{-3}$ are required if $M_k$ is as low as 1 TeV and the mass difference between $\eta_R$ and $\eta_L$ is kept around 1 GeV. Such a small mass splitting between $\eta_R$ and $\eta_L$ will correspond to small quartic coupling $\lambda_5 \sim 10^{-4}$. Thus, one can suitably choose the Yukawa couplings, quartic coupling $\lambda_5$ and $M_k$ in order to arrive at sub-eV light neutrino masses. To be in exact agreement with light neutrino masses, we first rewrite the neutrino mass given above in Eq. (5) in the form of type I seesaw formula

\[
M_v = y \tilde{M}^{-1} y^T, \tag{7}
\]

where we have introduced the diagonal matrix $\tilde{M}$ with elements

\[
\tilde{M}_i = \frac{2 \pi^2}{\lambda_5} \frac{2 M_i}{\xi_i v^2}, \tag{8}
\]

and

\[
\xi_i = \left( \frac{M_i^2}{8 (m_{\eta R}^2 - m_{\eta L}^2)} \right)^{-1} \left[ L_i (m_{\eta R}^2) - L_i (m_{\eta L}^2) \right]. \tag{9}
\]

The light neutrino mass matrix (7) is diagonalised by the usual Pontecorvo–Maki–Nakagawa–Sakata (PMNS) mixing matrix $U$, which is determined from the neutrino oscillation data (up to the Majorana phases):

\[
D_v = U^\dagger M_v U^* = \begin{pmatrix} m_1 & m_2 & m_3 \end{pmatrix}. \tag{10}
\]

Then the Yukawa coupling matrix satisfying the neutrino data can be written as

\[
y = U D^{1/2} \tilde{M}^{1/2}, \tag{11}
\]

where $O$ is an arbitrary complex orthogonal matrix. This is the equivalent of the Casas–Ibarra parametrisation [23] for scotogenic model [24].

3 Leptogenesis from annihilations

In the minimal scotogenic model discussed in the previous section, there are different types of annihilation processes which violate lepton number. They are namely,

1. annihilation process of scalar doublet $\eta$: $\eta \eta \rightarrow L_a L_b$.
2. coannihilation process of scalar doublet and one of the singlet fermions: $\eta N \rightarrow LX$ where $(X = h, \gamma, W^\pm, Z)$.

Interestingly, if we put the additional constraints that such lepton number violating annihilations and coannihilations also generate a non-zero CP asymmetry, they lead to two different DM possibilities namely,

1. the lightest neutral component of inert scalar doublet $\eta$ as DM,
2. the lightest right handed neutrino $N$ as DM.

The Boltzmann equations for leptonic asymmetry is given as follows:

\[
\frac{dY_{\Delta L}}{dz} = \frac{1}{\varepsilon H(z)} \times \sum_i \epsilon_{N_i} (Y_{N_i} - Y^{eq}_{N_i}) \Gamma_{N_i \rightarrow \Delta L}\eta
\]

\[
\text{F.L.} \tilde{R}_N \Gamma \tilde{N}_x \rightarrow \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x
\]

\[
\frac{1}{2} Y_{\Delta L} Y_{\eta}^{eq} \tilde{R}_N \Gamma \tilde{N}_x \rightarrow \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x
\]

\[
\sum_i \epsilon_{N_i} Y_{\eta} \eta \Gamma \tilde{N}_x \rightarrow \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x
\]

\[
\sum_i \epsilon_{N_i} Y_{\eta}^{eq} \tilde{R}_N \Gamma \tilde{N}_x \rightarrow \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x + \text{L.S.} \tilde{R}_N \Gamma \tilde{N}_x
\]
where $z = \frac{M_{DM}}{H(z)}$, $M_{PL}$ is the Planck mass and $Y = n/s$ denotes the comoving number density, as the ratio of number density to entropy density. The details of the derivation of this Boltzmann equation as well as the relevant equations for DM are presented in appendix A. In the above equation, $\epsilon_{\eta\eta}$ and $\epsilon_{N_i\eta}$ will be given appropriately later and $\epsilon_{N_i}$ is taken from [21].

$$
\begin{align*}
\epsilon_{N_i} &= \sum_\alpha \frac{1}{8\pi (y^{\alpha})_{ij}} \sum_{j \neq i} \left[ f \left( \frac{M_{N_i}^2}{M_{N_j}^2} \right) \frac{m_j^2}{M_s^2} \right] \Im \left[ \langle y_{\alpha i} \gamma_{\alpha j} (y^{\alpha})_{ij} \rangle \right] \\
&\quad - \frac{M_{N_i}^2}{M_{N_i}^2} \left( 1 - \frac{2}{M_{N_i}^2} \right)^2 \Im \left[ \langle y_{\alpha i} \gamma_{\alpha j} H_{ij} \rangle \right] \\
H_{ij} &= (y^{\alpha})_{ij} M_{N_i} M_{N_j} + (y^{\alpha})_{ij} M_{N_j} M_{N_i} \\
f(x, w) &= \sqrt{x} \left[ 1 + \frac{1 - 2w + x}{(1 - w)^2} \ln \left( \frac{x - w^2}{1 - 2w + x} \right) \right]
\end{align*}
$$

$M_{DM}$ in $s$ is the mass of $Z_2$ odd particle taken appropriately depending on the scenario mentioned above. Here $K_n$ is the $n$th order Modified Bessel function of second kind. The details of the Boltzmann equations are given in appendix A. We will now discuss this general framework in the context of two specific scenarios of DM mentioned above in the upcoming subsections.

The above Boltzmann equation contains the next leading order (NLO) contributions to lepton asymmetry. For usual type I seesaw leptogenesis, such NLO effects have been calculated already, for example, see [25] and references therein. It is therefore necessary to include or consider all the diagrams which can either contribute to lepton asymmetry or washout at the same order of couplings. We first only show the annihilation of dark sector particles into SM ones in Fig. 1 for the case of scalar doublet dark matter. We do not present the usual well-known two body decay diagrams (both tree and one loop) for simplicity. Based on the diagrams shown in Fig. 1, one can construct several other diagrams just by interchanging initial and final state particles. For example, it is straightforward to consider three body decay diagram of $N_i$ into $\eta, L, X \equiv \gamma, W^{\pm}, Z$. This diagram, which contributes to the asymmetry at order $O(y^4 g^2)$ will be suppressed due to not only phase space but also additional $O(g^2)$ suppression.

Now, although the 3-body decay and the co-annihilation are of the same order, the contribution in the Boltzmann evolution is different as they enter the Boltzmann equation differently. The 3-body decay will enter into the equation as an addition to the 2-body decay in which the contribution coming from the 2 body decay will dominate. As will be shown later, the contributions of coannihilation to lepton asymmetry may dominate over that from decay process. This is due to fact that the imaginary part of the interference is not suppressed as it becomes two $2 \rightarrow 2$ processes (referring to the diagrams in the second line in Fig. 2 leading to the interference at order $O(y^4 g^2)$) both mediated by the leptons after cutting loop diagrams, whereas in case of the decay the loop diagram becomes $1 \rightarrow 2$ and $2 \rightarrow 2$ in which the $2 \rightarrow 2$ is a $t$-channel process mediated by the right-handed neutrino after cutting. We present all such 1-loop diagrams contributing to the asymmetry arising from the interference at order $O(y^4 g^2)$ and $O(y^6)$ in Fig. 2. Similarly, there exists several washout processes that can be constructed by swapping initial and final state particles. This is true for fermion dark matter as well, which we discuss in one of the upcoming sections. To point out the significance of such processes at the same NLO, we therefore make a comparison of different washout processes (both inverse decay and scatterings) and show them in in Fig. 3 (lightest decay as Dark Matter) and in Fig. 6 (lightest fermion as Dark Matter).

### 3.1 Scalar doublet $\eta$ as dark matter

In this scenario the only way to get asymmetry is through co-annihilations. Pure scalar annihilations give rise to vanishing leptonic asymmetry if $\eta$ is the lightest $Z_2$ odd particle, as required for it to be the DM candidate. This is particularly due to the fact the “on-shell” criteria of loop particles can not be realised in such case, resulting in a vanishing CP asymmetry, as we discuss below.

The relevant coannihilation processes, both tree level as well as one loop level, are shown in Figs. 1 and in 2. One may notice that the one loop self-energy diagrams, arising
from the lepton propagator, do not contribute to the lepton asymmetry because the processes occur before electroweak symmetry breaking and thus lepton mass should be zero giving rise to vanishing self-energy loop contribution. Thus, only interference between tree and one loop vertex correction can give rise to CP asymmetry. For this scenario the Boltzmann equations for the $Z_2$ odd particles take the following form:

$$
\frac{dY_{N_k}}{dz} = -\frac{1}{zH(z)} \times \left[ (Y_{N_k} - Y_{N_k}^{eq}) (\Gamma_{N_k \to L_\alpha}) + (Y_{N_k} Y_\eta - Y_{N_k}^{eq} Y_{\eta}^{eq}) x (\sigma v)_{\eta N_k \to LSM} + \sum_{l=1}^{3} (Y_{N_k} Y_{N_l} - Y_{N_k}^{eq} Y_{N_l}^{eq}) x (\sigma v)_{N_l N_k \to SMSM} \right],
$$

$$
\frac{dY_{\eta}}{dz} = \frac{1}{zH(z)} \times \left[ (Y_{N_k} - Y_{N_k}^{eq}) (\Gamma_{N_k \to L_\alpha}) - 2(Y_\eta^2 - (Y_{\eta}^{eq})^2) x (\sigma v)_{\eta \eta \to SMSM} - \sum_{m=1}^{3} (Y_{N_m} Y_\eta - Y_{N_m}^{eq} Y_{\eta}^{eq}) x (\sigma v)_{\eta N_m \to LSM} \right].
$$

The CP asymmetry arising from the interference between tree and 1-loop diagrams in Figs. 1 and 2 can be estimated as

$$
\epsilon_{N_i \eta} = \frac{2}{(yy^\dagger)_{ii}} \sum_j \Im[(yy^\dagger)_{ij} \tilde{\epsilon}_{ij}],
$$

$$
\tilde{\epsilon}_{ij} = \frac{\sqrt{x_j}}{6x_i \left(-x_i^{3/2} + x_i(x_j - 2) + \sqrt{x_i}x_j + 1\right)^2} \left(\sqrt{x_i} - 3\right) \times \left(x_j^{3/2} (3x_j + 1) + \sqrt{x_i} (3x_j + 5) + 1\right) - 3x_j^{5/2} x_j (D + (x_j - 3)x_j + 4) - 3D - 2.
$$
\[-3x_i^{3/2}(2(D+3)+x_j(x_j(D+x_j+1)-D-4))
- x_i^3 + f^3(3D + 3x_j^2 + 11)\]
\[-3x_i^2(x_j(D+2(x_j-1)x_j+2)-D+6)\]
\[+x_i(1-3x_j(D+x_j-4))\]
\[+\sqrt{\frac{x_j}{4x_i}}(\sqrt{x_i}-1 + \frac{\sqrt{x_j}}{(1+\sqrt{x_i})^2}(\sqrt{x_i}-1 + r_j))\]
\[\times\left(\log\left(1+\sqrt{x_i x_j}\right)\right)\]
\[\frac{\sqrt{x_i x_j} \Gamma_j}{\pi(x_i-x_j)^2 + x_j \Gamma_j^2}\]
\[D = \sqrt{(x_i-x_j)(x_i+4\sqrt{x_i}-x_j+4)}\]
\[x_i = \frac{M_{\eta_i}^2}{m_{\eta}^2} \quad \Gamma_j = \frac{\gamma_j}{m_{\eta}}\]
by three complex parameters of type $\theta_{\alpha \beta} = \theta_{\alpha \beta}^R + i \theta_{\alpha \beta}^I$, $\theta_{\alpha \beta} \in [0, 2\pi]$, $\theta_{\alpha \beta}^R \in \mathbb{R}$ [26]. In general, the orthogonal matrix $O$ for $n$ flavours can be product of $nC_2$ number of rotation matrices of type
\[O_{\alpha \beta} = \begin{pmatrix}
\cos(\theta_{\alpha \beta}^R + i \theta_{\alpha \beta}^I) & \cdots & \sin(\theta_{\alpha \beta}^R + i \theta_{\alpha \beta}^I)
\vdots & \ddots & \vdots
-\sin(\theta_{\alpha \beta}^R + i \theta_{\alpha \beta}^I) & \cdots & \cos(\theta_{\alpha \beta}^R + i \theta_{\alpha \beta}^I)
\end{pmatrix},\]
with rotation in the $\alpha - \beta$ plane and dots stand for zero. For example, taking $\alpha = 1, \beta = 2$ we have
\[O_{12} = \begin{pmatrix}
\cos(\theta_{12}^R + i \theta_{12}^I) & \sin(\theta_{12}^R + i \theta_{12}^I) & 0
-\sin(\theta_{12}^R + i \theta_{12}^I) & \cos(\theta_{12}^R + i \theta_{12}^I) & 0
0 & 0 & 1
\end{pmatrix}\]
The above asymmetry along with this rotation (one at a time) takes the following form
\[\epsilon_{N_{i\eta}} = \sum_j \frac{(m_j^4-m_i^4)\sin(2\theta_{ij}^R)\sin(2\theta_{ij}^I)}{\Lambda_j^2(m_i^2-m_j^2)\cos(2\theta_{ij}^R)+(m_i^2+m_j^2)\cosh(2\theta_{ij}^I))}\times \tilde{e}_{ij},\]
where $m_i$’s are the light neutrino masses and $\Lambda_j$’s are defined above in Eq. (5). On the right hand side of the above equation, a summation over index $j$ is implicit. As an example, we have taken the benchmark values shown in Table 1 to compute the baryon asymmetry as well as scalar DM relic numerically. Here we consider $\eta_I$ as the DM candidate ($\eta_I \equiv$ DM, corresponding to positive value of quartic coupling $\lambda_3$) which is similar to the inert doublet model discussed extensively in the literature [19,28,29]. Typically there exists two distinct mass regions, $M_{\text{DM}} \leq 80$ GeV and $M_{\text{DM}} \geq 500$ GeV, where correct relic abundance criteria can be satisfied. In both regions, depending on the mass differences $m_{\eta^+} - m_{\eta_I}$, $m_{\eta_R} - m_{\eta_I}$, the coannihilations of $\eta_I, \eta^\pm$ and $\eta_R, \eta_I$ can also contribute to the DM relic abundance [30,31]. As for the mixing angles in the PMNS matrix $U$ we took the best fit values obtained from the recent global fit analysis [32] shown in Table 2.

To perform the numerical analysis, we implement the model in SARAH 4 [33] and extract the thermally averaged annihilation rates from micrOMEGAs 4.3 [34] to use while solving the Boltzmann equations above. In Fig. 3, we plot the comoving number densities of all $Z_2$ odd particles, taking part in generating the lepton asymmetry along with the generated asymmetry $\Delta L$, as functions of temperature. The

1 For some more discussions on different possible structure of this matrix and implications on a particular leptogenesis scenario in this model, we refer to the recent work [27].
left panel corresponds to normal hierarchy (NH) of neutrino mass spectrum and the right panel to the case of inverted hierarchy (IH). The horizontal solid black line labelled as “ΔL observed” correspond to the value of ΔL that is partially converted into the observed baryon asymmetry via the electroweak sphaleron processes with the conversion factor C_{sph} = \frac{8N_f^2 + 4N_H^2}{\pi^2 N_f + 4N_H^2}, where N_f = 3, N_H = 2 are the number of fermion generations and Higgs doublets respectively [35]. While sphalerons violate B + L, they conserve B − L symmetry. The sphaleron processes are effective with a thermal rate \Gamma_{\text{sph}} \sim (\alpha_T)^4 with SU(2) gauge coupling constant \alpha_T at high temperature until EW phase transition, while they are exponentially suppressed due to finite gauge boson masses after EW gauge symmetry breaking. The shaded regions in the panels correspond to the temperature below which the sphaleron processes become inoperative(T \lesssim 200 \text{ GeV}) [36]). The benchmark parameters are chosen in such a way that the generated lepton asymmetry ΔL by the epoch of sphaleron freeze-out is sufficient enough to produce the observed baryon asymmetry. The dashed horizontal black line corresponds to the observed DM relic abundance in the present universe [1]. As can be seen from this plot, the lepton asymmetry grows as the temperature cools down due to the contributions from the co-annihilation diagrams. While the lepton asymmetry gets converted into the baryon asymmetry at EW phase transition temperature, it takes a while for DM to freeze-out. Since non-zero CP asymmetry arises from coannihilations between η and heavier right handed neutrinos N_{2,3}, the lepton number generating processes get frozen out much earlier compared to DM self annihilations. This makes sure that a net lepton asymmetry is created with the right amount without being washed out entirely. The limits on the parameter \lambda_5, keeping all the other parameters same as shown on Table 1, are set by two constraints. One is the mass difference between the neutral scalar and pseudo-scalar (Δ = m_{\eta_R} - m_{\eta_I}) which needs to be more than approximately 100 \text{ keV}, in order to avoid Z mediated inelastic direct detection scattering of DM off nucleons, as we discuss below. The other constraint is coming from the required leptonic asymmetry with maximal CP asymmetry. The range is shown in Table 3.

Since the DM in this scenario has electroweak gauge interactions, we include DM direct detection constraints arising from tree level Z boson mediated processes \eta_R n \rightarrow \eta_I n, n being a nucleon (shown in Fig. 4). The cross section for Z mediated inelastic process is \cite{38}
\begin{equation}
\sigma_n^0 = \frac{G_F^2}{2\pi} m_n^2 \sim 7.44 \times 10^{-39} \text{cm}^2.
\end{equation}
We note that one can forbid such scattering if δ = m_{\eta_I} - m_{\eta_R} > 100 \text{ keV}. Using the expressions for physical masses above, it leads to a lower bound on the dimensionless quartic coupling \lambda_5 as
Fig. 3  Top panel: comoving number densities of $Z_2$ odd particles and lepton asymmetry as a function of temperature for scalar DM scenario. The left (right) panel corresponds to the normal (inverted) hierarchy of neutrino mass spectrum. Bottom panel: rates of individual wash-out processes along with the Hubble rate (left panel); individual (co)annihilation contributions of each channel to the asymmetry. The solid (dashed) black line corresponds to the baryon asymmetry (DM abundance) observed at present epoch ($T \sim 0$). Shaded regions represent the epochs after sphaleron freeze out

$$\lambda_5 \approx 1.65 \times 10^{-7} \left( \frac{\delta}{100 \text{ keV}} \right) \left( \frac{M_{\text{DM}}}{100 \text{ GeV}} \right).$$

This lower limit on $\lambda_5$ becomes weaker for heavier DM masses. Now, if we avoid this bound i.e the mass difference between the scalar and pseudo-scalar dark matter is above 100 keV then the direct detection is majorly dominated by the first process shown in Fig. 4. Our benchmark point satisfies this constraint, forbidding such inelastic DM scattering. The Yukawa couplings for all three generation of leptons for the chosen benchmark point (considering only 13 rotation in $O$ matrix, however) in this scenario can be written in terms of the following matrix.

$$y|_{NH} = \begin{pmatrix} 4.47 - 5.04 i & 10.7 + 4.77 i & 6.35 + 7.96 i \\ -0.66 - 5.30 i & 8.38 - 4.06 i & 7.29 + 0.59 i \\ -6.34 - 2.74 i & 1.15 - 11.7 i & 6.20 - 8.2 i \end{pmatrix} \times 10^{-3},$$

$$y|_{IH} = \begin{pmatrix} 8.52 - 13.8 i & 5.78 + 0.25 i & -5.66 - 0.20 i \\ -4.89 - 12.8 i & 4.54 - 3.93 i & -4.42 + 4.03 i \\ -17.18 - 3.51 i & -2.6 - 6.78 i & 2.71 + 6.60 i \end{pmatrix} \times 10^{-3}.$$

$\copyright$ Springer
If the lightest 2 odd particle is the lightest of the right handed neutrinos (and hence the DM candidate), then the annihilation processes responsible for creating a non-zero lepton asymmetry are shown in Fig. 5. Once again, pure self annihilation of DM can not provide the asymmetry due to the absence of “on-shell” condition for loop particles. If the scalar doublet $\eta$ is the next to the lightest $Z_2$ odd particle, then the annihilation processes shown in Fig. 5 can produce the required lepton asymmetry. For this scenario the Boltzmann equations for the $Z_2$ odd particles take the following form:

$$
\frac{dY_{N_k}}{dz} = -\frac{1}{zH(z)} \times \left[ \left( Y_{N_k} - Y_{N_k}^{eq} \right)(\Gamma_{N_k\rightarrow L\eta}) 
+ \left( Y_{N_k} - Y_{N_k}^{eq} \right) Y_{\eta}^{eq} \sigma v Y_{\eta}^{eq} N_{k\rightarrow LSM} 
+ \sum_{l=1}^{3} \left( Y_{N_k} - Y_{N_k}^{eq} \right) Y_{\eta}^{eq} \sigma v Y_{\eta}^{eq} N_{l\rightarrow LSM} \right],
$$

for $k = 2, 3$

$$
\frac{dY_{\eta}}{dz} = \frac{1}{zH(z)} \times \left[ \left( Y_{\eta} - Y_{\eta}^{eq} \right)(\Gamma_{\eta\rightarrow L\eta}) 
- Y_{\eta}^{eq} \sigma v Y_{\eta}^{eq} \eta_{N\rightarrow LSM} 
- 2(Y_{\eta}^{eq})^2 \sigma v Y_{\eta}^{eq} \eta_{N\rightarrow LSM} 
- \sum_{m=1}^{3} \left( Y_{N_m} N_{\eta} - Y_{N_m}^{eq} \right) \sigma v Y_{\eta}^{eq} N_{m\rightarrow LSM} \right],
$$

$$
\frac{dY_{N_1}}{dz} = \frac{1}{zH(z)} \times \left[ \left( Y_{N_1} - Y_{N_1}^{eq} \right)(\Gamma_{N_1\rightarrow L\eta}) 
- Y_{N_1} \sigma v Y_{N_1}^{eq} \eta_{N_1\rightarrow LSM} 
- 2(Y_{N_1}^{eq})^2 \sigma v Y_{N_1}^{eq} \eta_{N_1\rightarrow LSM} 
- \sum_{l=1}^{3} \left( Y_{N_1} Y_{N_l} - Y_{N_1}^{eq} \right) \sigma v Y_{N_l}^{eq} N_{l\rightarrow LSM} \right].
$$

(23)
The washout effects in this scenario are categorised as follows:

- **ΔL = 2**: there are two processes of this type:
  1. $\eta \eta \rightarrow LL$ and $L \eta \rightarrow L \eta$ where the former is also responsible for the source of asymmetry while the latter is purely wash-out.
  2. the inverse of co-annihilation $N_k \eta \rightarrow L, X = (\gamma, W, h)$

In Fig. 6, we plot the predictions for relic abundance of all $Z_2$ odd particles, taking part in generating the lepton asymmetry along with the generated asymmetry $\Delta L$, as functions of temperature, for fermion DM scenario. The upper left panel corresponds to the NH of neutrino masses, whereas the upper right panel to the IH of neutrino masses. In the lower panel, we compare the relative contributions to the lepton asymmetry: from $\eta - \eta$ annihilations $(\Delta L_{\eta})$, from $\eta - N_k$ coannihilations $(\Delta L_{N_{\eta}})$, from $N_2$ decay $(\Delta L_N)$, as functions of temperature. Similar to the scenario of scalar DM, here also the lepton asymmetry grows as temperature cools due to contributions from the annihilations and coannihilations and saturate around the temperature where the processes responsible for creating the asymmetry tend to go out of equilibrium. Also, the lightest right handed neutrino freezes out to give the required relic abundance for DM in the universe. The shaded regions in the panels correspond to the temperature below which the sphaleron processes become inoperative.

The first bump in the curve for the lepton asymmetry shown in upper panel plots of Fig. 6 arises from the coannihilation diagrams while the decay contribution enters later and further increases the asymmetry at later stages. Here we notice that the mass of the lightest right handed fermion is very close to the $Z_2$ odd scalar counterparts in order to enhance the coannihilations. This is evident from the bottom panel plot of Fig. 6 which shows the co-annihilation among the lightest $N$ and $Z_2$ odd scalar components contribute dominantly to lepton asymmetry. Along with that we have an interesting feature of $\lambda_5$. In this we have seen that for particular parameter set as shown in Table 5, the upper bound on $\lambda_5$ is set by the requirement of the required lepton asymmetry needed to explain the observed baryonic asymmetry in the Universe and the lower bound is set by the Lepton flavor violating process $BR(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ \cite{39}, as we discuss below. Since the dark matter candidate is a fermion singlet in this case, the parameter $\lambda_5$ is not constrained by dark matter direct detection. While there exist some washout effects for the coannihilating processes, there is not much of that for the annihilation processes, as the processes are already out of equilibrium when wash-out becomes effective. In this case, large Yukawa couplings are required to achieve successful leptogenesis, which in turn leads to very small $\lambda_5$, but yet does not affect fermion DM phenomenology much. The Yukawa couplings can be represented by the following matrix for the chosen benchmark point in this scenario.

$$y |_{NH} = \begin{pmatrix} 1.01 - 1.14i & 2.43 + 1.09i & 1.44 + 1.8i \\ -0.15 - 1.21i & 1.92 - 9.29i & 1.67 + 0.13i \\ -1.40 - 0.61i & 2.55 - 2.6i & 1.37 - 1.81i \end{pmatrix} \times 10^{-2}, \quad (26)$$

$$y |_{IH} = \begin{pmatrix} 1.88 - 3.05i & 1.28 + 0.55i & -1.25 - 0.45i \\ -1.12 - 2.92i & 1.04 - 0.9i & -1.01 + 0.92i \\ -3.87 - 0.79i & -0.59 - 1.53i & 0.61 + 1.49i \end{pmatrix} \times 10^{-2}. \quad (27)$$

We then use the SPheno 3.1 \cite{37} interface to check the constraints from flavour data. We particularly focus on
Fig. 6 Top panel: comoving number densities of $Z_2$ odd particles and lepton asymmetry as a function of temperature for fermion DM scenario. The left (right) panel corresponds to the normal (inverted) hierarchy of neutrino mass spectrum. Bottom panel: rates of individual wash-out processes along with the Hubble rate (left panel); individual (co)annihilation contributions of each channel to the asymmetry. The solid (dashed) black line corresponds to the baryon asymmetry (DM abundance) observed at present epoch ($T \sim 0$). Shaded regions represent the epochs after sphaleron freeze out.

Three charged lepton flavour violating (LFV) decays namely, $\mu \rightarrow e\gamma$, $\mu \rightarrow 3e$ and $\mu \rightarrow e$ (Ti) conversion that have strong current limit as well as good future sensitivity [24]. The present bounds are: $\text{BR}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$ [39], $\text{BR}(\mu \rightarrow 3e) < 1.0 \times 10^{-12}$ [40], $\text{CR}(\mu, \text{Ti} \rightarrow e, \text{Ti}) < 4.3 \times 10^{-12}$ [41]. While the future sensitivity of the first two processes are around one order of magnitude lower than the present branching ratios, the $\mu$ to $e$ conversion (Ti) sensitivity is supposed to increase by six order of magnitudes [24] making it a highly promising test to confirm or rule out different TeV scale BSM scenarios. It should be noted that such charged LFV process arises in the SM at one loop level and remains suppressed by the smallness of neutrino masses, much beyond the current and near future experimental sensitivities. Therefore, any experimental observation of such processes is definitely a sign of BSM physics, like the one we are studying here. We show the predictions for LFV processes in our model in Fig. 7, also highlighting the second benchmark point (BP2) mentioned above. The similar contributions for the BP1 scenario remain far more suppressed due to smallness of the corresponding Yukawa couplings. The scatter plot in Fig. 7 is obtained by only varying $\mu_\eta$ from 100 GeV to 1 TeV, and fixing the other parameters with the values presented in Table 4. It can be seen that some part of the
Fig. 7 Predictions for LFV processes for $10^2 \text{ GeV} < M_{\text{DM}} < 10^3 \text{ GeV}$. The two benchmark points are highlighted with red and blue coloured points. The $\mu_\nu$ are varied from 100 GeV to 1 TeV, and the other parameters are taken as presented in Table 4.

4 Conclusion

We have proposed a scenario where baryogenesis via leptogenesis can be achieved through annihilations and coannihilations of particles belonging to a $Z_2$ odd sector including t-channel processes. We have considered a popular model known as the scotogenic model to implement the idea, and addressed the possibility of explaining the coincidence of DM abundance and baryon asymmetry in the present universe along with non-zero neutrino masses. Pointing out two different possible scenarios corresponding to scalar and fermion DM respectively, we show the non-trivial role played by t-channel annihilation as well as coannihilation processes between different $Z_2$ odd particles. For the two benchmark points chosen in our work, we could obtain successful leptogenesis along with other requirements like DM relic, DM direct detection and light neutrino masses for $M_{\text{DM}} \sim 870$ GeV whereas vanilla leptogenesis in scotogenic model works for $M_1 \geq 10^{10}$ TeV. Another interesting feature is the testability of the model at DM direct detection and rare decay experi-
ments. Even though the particle spectrum is in a few $O(100)$ GeV regime or above, away from the reach of current collider experiments, the model can still be tested at near future run of rare decay experiments looking for charged lepton flavour violation like $\mu \rightarrow e\nu$, $\nu \rightarrow 3e$, $\mu \rightarrow e$ conversion etc. We highlight our interesting results by adopting benchmark points here and leave a detailed numerical analysis of this scenario to an upcoming work.

Acknowledgements One of the authors, DB acknowledges the hospitality and facilities provided by School of Liberal Arts, Seul-Tech, Korea where this work was completed. SK and AD were supported by the National Research Foundation of Korea (NRF) Grants (2017K1A3A7A09016430, 2017R1A2B4006338).

Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors’ comment: The figures and tables are enough to present out results, that’s why there is no data.]

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

Funded by SCOAP3.

Appendix A: Details of the Boltzmann Equations

In this section, we present the Boltzmann Equation (BE) used in our analysis, in detail. The standard BE is written as follows:

$$
\frac{dX_\alpha}{dz} = \Delta n_\alpha \frac{X_{i_1} X_{i_2} \cdots}{s H(z) z} \gamma_{eq} \times (i_1 + i_2 \cdots \rightarrow f_1 + f_2 + \cdots),
$$

(A1)

where $X_\alpha = n_\alpha/s$ is the comoving number density, $z = M_r/T$ ($M_r$ is the reference scale which is same as the mass of the decaying particle in usual leptogenesis/baryogenesis while being equal to the mass of dark matter in the case of dark matter freeze-out ) and $\Delta n_\alpha$ is the change of number of particle in the process considered. Along with that, the Hubble expansion rate, $H(z)$, and entropy density, $s$, are defined respectively as

$$
H(z) = \sqrt{\frac{4\pi^3 g_*}{45} \frac{T^2}{M_{pl}}} = \sqrt{\frac{4\pi^3 g_*}{45} \frac{M_r^2}{M_{pl}^2 z^2}} = \frac{H(M_r)}{z^2},
$$

(A2)

$$
s = g_* \frac{2\pi^2}{45} T^3.
$$

(A3)

Now, the collision term $\gamma_{eq}(i_1 + i_2 \cdots \rightarrow f_1 + f_2 + \cdots)$ are of two types: 1) decay and 2) annihilation processes. For decay process it is given as:

$$
\gamma_{D}^{eq}(i \rightarrow f_1 + f_2 + \cdots) = \frac{g_{i} m_{i}^{2}}{2\pi^{2}} T K_{1}(M_{i}/T) \Gamma(i \rightarrow f_1 + f_2 + \cdots),
$$

(A4)

and for the scattering processes it is given as

$$
\gamma_{s}^{eq}(i_1 + i_2 \rightarrow f_1 + f_2 + \cdots) = \frac{g_{s} g_{s_{i_{1}}} T}{64\pi^{4}} \int_{s_{min}}^{\infty} \frac{2\lambda(s, m_{1}^{2}, m_{2}^{2})}{s} \sigma \sqrt{s} K_{1}(\sqrt{s}/T),
$$

(A5)

where $K_n$ is the nth order Modified Bessel function of second kind, $\lambda(a, b, c) = a^2 + b^2 + c^2 - 2ab - 2ac - 2bc$ and $s_{min} = \text{Max}((m_{i_{1}} + m_{i_{2}})^2, (m_{f_{1}} + m_{f_{2}} + \cdots)^2)$.

Now, we present the explicit expressions of the BEs for $N_k$ and $\eta$ in the case of scalar dark matter.

$$
\frac{dY_{N_k}}{dz} = - \frac{1}{s z \eta H(z)} \times \left[ \left( \frac{Y_{N_k}}{Y_{N_k}} - 1 \right) \gamma_{D}(N_k \rightarrow L_\alpha \eta) + \left( \frac{Y_{N_k}}{Y_{N_k}} - 1 \right) \gamma_{s}^{eq}(\eta N_k \rightarrow \text{SM}) \right],
$$

(A6)

And similarly expressions of BEs for $N_k$ and $\eta$ in the case of fermion dark matter.

$$
\frac{dY_{\eta}}{dz} = - \frac{1}{s z \eta H(z)} \times \left[ \left( \frac{Y_{\eta}}{Y_{\eta}} - 1 \right) \gamma_{D}(\eta \rightarrow L_\alpha \eta) + \left( \frac{Y_{\eta}}{Y_{\eta}} - 1 \right) \gamma_{s}^{eq}(\eta N_m \rightarrow \text{SM}) \right].
$$


\[ \begin{align*}
&+ \frac{3}{s \eta H(z)} \sum_{k=1}^{3} \left( Y_{N_k} Y_{N_k} \frac{\gamma_{\alpha N_k}}{Y_{\eta N_k}} - 1 \right) \gamma_{\alpha}^\text{eq} (N_k \rightarrow \text{LSM}) \right]. \\
\text{for } k = 2, 3 \\
&dY_{N_1} \over dz = \frac{1}{s \eta H(z)} \left[ \left( \frac{Y_{N_1}}{Y_{\eta N_1}} - 1 \right) \gamma_{\alpha}^\text{eq} (\eta N_1 \rightarrow \text{LSM}) \\
&- \frac{3}{s \eta H(z)} \sum_{k=1}^{3} \left( Y_{N_k} Y_{N_k} \frac{\gamma_{\alpha N_k}}{Y_{\eta N_k}} - 1 \right) \gamma_{\alpha}^\text{eq} (N_k \rightarrow \text{LSM}) \right].
\end{align*} \]

\[ \begin{align*}
&\frac{dY_{\eta}}{dz} = \frac{1}{s \eta H(z)} \left[ \sum_{k=2}^{3} \left( Y_{N_k} Y_{N_k} \frac{\gamma_{\alpha N_k}}{Y_{\eta N_k}} - 1 \right) \gamma_{\alpha}^\text{eq} (N_k \rightarrow \text{LSM}) \\
&- \frac{3}{s \eta H(z)} \sum_{m=1}^{3} \left( Y_{N_m} Y_{N_m} \frac{\gamma_{\alpha N_m}}{Y_{\eta N_m}} - 1 \right) \gamma_{\alpha}^\text{eq} (N_m \rightarrow \text{LSM}) \right].
\end{align*} \]

Finally the expressions of BEs for the lepton numbers as follows:

\[ \begin{align*}
&\frac{dY_{\eta}}{dz} = \frac{1}{s \eta H(z)} \left[ \sum_{j} \left( \frac{Y_{N_j}}{Y_{\eta N_j}} - \frac{Y_{L_j}}{Y_{\eta L_j}} \right) (1 + \epsilon_{N_j}) \gamma_{\alpha}^\text{eq} (N_j \rightarrow \text{LSM}) \\
+ 2 \left( \frac{Y_{N_j}^2}{(Y_{\eta N_j})^2} - \frac{Y_{L_j}^2}{(Y_{\eta L_j})^2} \right) (1 + \epsilon_{\eta j}) \gamma_{\alpha}^\text{eq} (\eta j \rightarrow \text{LL}) \\
+ \sum_{i} \left( \frac{Y_{N_i} Y_{N_i}}{Y_{\eta N_i} Y_{\eta L_i}} - \frac{Y_{L_i} Y_{L_i}}{Y_{\eta L_i} Y_{\eta L_i}} \right) (1 + \epsilon_{N_i}) \gamma_{\alpha}^\text{eq} (N_i \rightarrow \text{LSM}) \right. \\
\left. + \sum_{i} \left( \frac{Y_{N_i} Y_{N_i}}{Y_{\eta N_i} Y_{\eta L_i}} - \frac{Y_{L_i} Y_{L_i}}{Y_{\eta L_i} Y_{\eta L_i}} \right) (1 + \epsilon_{\eta L_i}) \gamma_{\alpha}^\text{eq} (\eta L_i \rightarrow \text{LL}) \right].
\end{align*} \]

where the leptonic comoving number density are defined as \( Y_{\eta L} = Y_{\eta L}^\text{eq} + Y_{\Delta L}/2 \), \( Y_{\eta X} = Y_{\eta X}^\text{eq} - Y_{\Delta L}/2 \). The rates \( \gamma_{\alpha}^\text{eq} (N_j \rightarrow \text{LSM}) \) and \( \gamma_{\alpha}^\text{eq} (\eta \rightarrow \text{LL}) \) are shown in Fig. 5, whereas \( \gamma_{\alpha}^\text{eq} (\eta \rightarrow \text{LSM}) \) and \( \gamma_{\alpha}^\text{eq} (N_i X \rightarrow \eta L) \) are shown in Fig. 1. The processes \( \gamma_{\alpha}^\text{eq} (N_i X \rightarrow \eta L) \) and \( \gamma_{\alpha}^\text{eq} (\eta X \rightarrow N_i L) \) are the same as Fig. 1 by just interchanging the one of the initial with the final particle. And finally the processes \( \gamma_{\alpha}^\text{eq} (\eta L \rightarrow \eta L) \) and \( \gamma_{\alpha}^\text{eq} (\eta \rightarrow N_i L) \) are shown in Fig. 8. There are no other further processes which contributes in the above Boltzmann equation. Now taking the difference between Eq. (A8) and Eq. (A9) and keeping the terms asymmetry to leading order i.e \( Y_{LL}^2 \simeq (Y_{LL}^\text{eq})^2 + Y_{LL}^\text{eq} Y_{\Delta L} \), one would get the final Boltzmann equation for asymmetry Eq. 12.

\[ \begin{align*}
&dY_{\Delta L} \over dz = \frac{1}{s \eta H(z)} \left[ \sum_{j} \left( \frac{Y_{N_j}}{Y_{\eta N_j}} - 1 \right) \epsilon_{N_j} \gamma_{\alpha} (N_j \rightarrow \text{LSM}) \right].
\end{align*} \]
Now, starting with the tree level amplitudes

\[ M_0 = \frac{x_0^\gamma(p_1 + p_2)\sigma y_N^\gamma(2p_1 - p_3)^\mu + im_\eta^2(t - m^2_\eta)}{s}, \]  

(B2)

where the amplitude \( M_0 \) corresponds to the tree diagram shown in Fig. 1. The corresponding amplitudes for the loop correction are given as follows

\[ M_1 = \frac{x_0^\gamma(p_1 + p_2)\sigma p_1 \sigma x_N m_N}{s} C_1 \]

\[ + \frac{x_0^\gamma(p_1 + p_2)\sigma p_2 \sigma x_N m_N}{s} C_2 \]

\[ + \frac{x_0^\gamma(2p_1 - p_3)^\mu}{(t - m^2_\eta)} C_3 \]

(B3)

The cross term coming from the above two expressions will give us

\[ \Im[A_0, A_1] |\Psi|^2 = \left[ m_N m_N \left( 2m_N^2 + s(s + t) - m_N^2 (2m_N^2 + 3s + 2t) \right) \right] \Im[C_1] \]

\[ + 2m_N m_N \frac{(t - m^2_\eta)}{s} \Im[C_2] \]

\[ + \left[ m_N^4 + t(2m_N^2 - s) - m_N^2 (2m_N^2 + 3s + 2t) \right] \Im[C_3] \]

The Appendix B: Details of the asymmetry

In this section we give the details of the asymmetry shown in Eq. (B9). We would first start with the the basic general expression giving the asymmetry shown as follows:

\[ \delta = 4 \Im[C^* C_1] \Im[A_0, A_1] |\Psi|^2, \]  

(B1)

where \( |\Psi| \) corresponds to the wavefunction of the incoming and outgoing particles, \( C^* \) corresponds to the couplings of the tree (\( C_0 \)) and loop (\( C_1 \)) and \( A^* \) corresponds to the rest of the amplitude respectively.
where

\begin{align*}
C_1 &= \frac{(s - m_v^2 - m_N^2)}{D} \\
&\times \left[ B_0(m_v^2, 0, m_N^2) - B_0(s, m_N^2, m_v^2) \\
&+ (m_v^2 - m_N^2)C_0 \\
&+ (m_v^2, m_N^2, (m_v^2 + m_N^2 - s)/2, 0, m_v^2, m_N^2) \right], \\
&\times \left[ B_0(s, m_N^2, m_v^2) - B_0(m_N^2, 0, m_v^2) \\
&+ (m_N^2 - m_v^2)C_0 \\
&+ (m_N^2, m_v^2, (m_N^2 + m_v^2 - s)/2, 0, m_N^2, m_v^2) \right], \\
&\times \left[ B_0(m_v^2, 0, m_N^2) - B_0(s, m_N^2, m_v^2) \\
&+ (m_v^2 - m_N^2)C_0 \\
&+ (m_v^2, m_N^2, (m_v^2 + m_N^2 - s)/2, 0, m_v^2, m_N^2) \right],
\end{align*}

\begin{align*}
C_2 &= \frac{(s - m_v^2 - m_N^2)}{D} \\
&\times \left[ B_0(s, m_N^2, m_v^2) - B_0(m_N^2, 0, m_v^2) \\
&+ (m_N^2 - m_v^2)C_0 \\
&+ (m_N^2, m_v^2, (m_N^2 + m_v^2 - s)/2, 0, m_N^2, m_v^2) \right], \\
&\times \left[ B_0(0, m_v^2, m_N^2) - B_0(s, m_v^2, m_N^2) \\
&+ (m_v^2 - m_N^2)C_0 \\
&+ (m_v^2, m_N^2, (m_v^2 + m_N^2 - s)/2, 0, m_v^2, m_N^2) \right], \\
&\times \left[ B_0(t, 0, m_N^2) - B_0(m_N^2, m_v^2, 0) \\
&+ (m_N^2 - m_v^2 + t - m_v^2)C_0 \\
&+ (m_N^2, m_v^2, (m_N^2 - t)/2, m_v^2, m_N^2, 0) \right], \\
D &= (s - m_v^2 - m_N^2)^2 - 4m_v^2m_N^2).
\end{align*}

Now the thermally averaged cross section is given as

\begin{equation}
\langle \sigma v \rangle = \frac{T}{32\pi m_v^2 m_N^2 K_2(m_v^2/T) K_2(m_N^2/T)}.
\end{equation}

References

1. Planck Collaboration, N. Aghanim et al., Planck 2018 results. VI. Cosmological parameters. arXiv:1807.06209
2. S. Weinberg, Cosmological production of Baryons. Phys. Rev. Lett. 42, 850–853 (1979)
3. E.W. Kolb, S. Wolfram, Baryon number generation in the early universe. Nucl. Phys. B 172, 224 (1980). [Erratum: Nucl. Phys. B 195, 542 (1982)]
4. M. Fukugita, T. Yanagida, Baryogenesis without grand unification. Phys. Lett. B 174, 45–47 (1986)
