Majorana neutrinos production at LHeC in an effective approach

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Abstract

We investigate the possibility of detecting Majorana neutrinos at the Large Hadron-electron Collider, an electron-proton collision mode at CERN. We study the $l_j^+ + 3\text{jets}$ ($l_j \equiv e, \mu, \tau$) final states that are, due to leptonic number violation, a clear signature for intermediate Majorana neutrino contributions. Such signals are not possible if the heavy neutrinos have Dirac nature. The interactions between Majorana neutrinos and the Standard Model particles are obtained from an effective Lagrangian approach. We present our results for the total cross section as a function of the neutrino mass, the effective couplings and the new physics scale. We also show the discovery region as a function of the Majorana neutrino mass and the effective couplings. Our results show that the LHeC may be able to discover Majorana neutrinos with masses lower than 700 and 1300 GeV for electron beams settings of $E_e = 50$ GeV and $E_e = 150$ GeV, respectively.

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I. INTRODUCTION

The discovery at the LHC of a new neutral boson has been a great scientific achievement for particle physics, and up to now no new physics has been found involving the electroweak scalar sector [1, 2]. Yet, it is well-known that the Standard Model (SM) -based on the gauge group $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$ undergoing a spontaneous symmetry breaking in its electroweak sector, up to the universal $U(1)_{EM}$ -leaves important questions unexplained. In the recent years, the first discovery of physics beyond minimum SM has taken place through the observation of flavor neutrino oscillations. This also has led to nonzero neutrino masses below or of the order of an electron volt [3]. Considering this scenario, physics at new colliders should probe not only the mechanism behind electroweak symmetry breaking and the stabilization of the electroweak scale, but also trace the existence and nature of neutrino masses. The recent Large Hadron-electron Collider (LHeC) proposal [4], an electron-proton collider at CERN, could serve both purposes.

Neutrino masses are difficult to generate in a natural way in the SM Yukawa interactions framework, and a very attractive and well-known scheme to obtain them is the seesaw mechanism, which requires the presence of heavy right-handed neutrino species of the Majorana type that allow for lepton number violation (LNV) [5–8]. The discovery of Majorana neutrinos would have profound theoretical implications in the formulation of a new model framework, while yielding insights into the origin of mass itself. Observation of any LNV process would be of great impact on particle physics and cosmology as, if neutrinos are Majorana particles, they may fit into the leptogenesis scenario for creating the baryon asymmetry, and hence the ordinary matter of the Universe [9]. However, the minimal seesaw framework generally leads to the decoupling of the Majorana neutrinos, and the observation of any LNV signal would indeed point toward new physics beyond the minimal seesaw models [10]. In this work we will investigate the possibility of discovering Majorana neutrinos at the LHeC, considering its interactions in a general and model-independent effective Lagrangian approach.

The seesaw mechanism, among other SM extensions, requires one or more extra right-handed neutrinos $\nu_R$ with a mass term

$$\mathcal{L}^{mass} = -\frac{1}{2} \bar{\nu}_R M \nu_R - \bar{L} \tilde{\phi} Y \nu_R + h.c. ,$$

(1)

where $L$ denotes the left-handed lepton doublet, $Y$ denotes the Yukawa coupling matrix, $\phi$
denotes the Higgs doublet and $M$ denotes the Majorana neutrino mass.

The diagonalization of the mass term gives

$$m_\nu = m_D M^{-1} m_D^T, \quad \text{with} \quad m_D = Y \frac{v}{\sqrt{2}},$$

(2)

and a mixing angle $U_{iN} \sim m_D/M$ between the light and the heavy Majorana neutrinos $N$.

The mixing angle $U_{iN}$ weighs the coupling of $N$ with the SM particles and in particular

with the charged leptons through the $V - A$ interaction:

$$\mathcal{L}_W = - \frac{g}{\sqrt{2}} U_{iN} \bar{N} c \gamma^\mu P_L W^+_{\mu} + h.c.$$  

(3)

In typical seesaw scenarios, the Dirac mass terms are expected to be around the electroweak scale ($m_D \sim m_W$) in order to have Yukawa couplings $Y \sim O(1)$ in Eq.(2), whereas the Majorana mass $M$ -being a singlet under the SM gauge group- may be very large, close to the grand unification scale. Thereby, the seesaw mechanism can explain the smallness of the observed light neutrino masses ($m_\nu \sim 0.01$ eV) while leading to the decoupling of $N$. Even a different choice in which $M \sim 100$ GeV and $m_D \sim 0.1$ $m_e$, keeping $m_\nu \sim 0.01$ eV, implies a vanishing mixing angle $U_{iN} \sim 10^{-7}$ [10]. This effect is so weak that the observation of LNV must indicate new physics beyond the minimal seesaw mechanism, as was indicated in Ref.[10].

In view of the above discussion, in this work, we consider -in a model-independent way- the effective interactions of the Majorana neutrino $N$ with a mass value lower than the new physics scale $\Lambda$ and a negligible mixing to $\nu_L$. In the case that heavy neutrinos do exist, present and future experiments will be capable of determining their nature. In particular, the production of Majorana neutrinos via $e^+e^-$, $e^-\gamma$, $\gamma\gamma$ and hadronic collision have been extensively investigated in the past [10] [13] [24].

In this paper we study the possibility for an $e^-p$ collider at CERN (LHeC) in order to produce clear signatures of Majorana neutrinos in the context of interactions coming from an effective Lagrangian approach. We study the lepton number violating reaction $e^-p \rightarrow l^+_j + 3 jets$ ($l_j \equiv e, \mu, \tau$) which receives contributions from the diagrams from the processes depicted in Fig.1. We have not considered the pure lepton decay channels because they involve light neutrinos that escape detection, in which case the Majorana nature of the heavy neutrinos would have no effect on the signal, since we should be able to know whether the final state contains neutrinos or antineutrinos.
The lepton number violating process studied here was previously investigated in Refs. [25, 26], for the type-I seesaw mechanism, focusing on the DESY experiment and extended to the LEP and LHC. Recent studies of the seesaw model at lepton-proton colliders like the LHeC were performed in Refs. [27, 28].

The principal advantage of electron-proton collisions with respect to hadron colliders is the cleanness of the signal. In the case of the LHeC, the leptonic number violation by 2 units is ensured by the presence of a final antilepton. Conversely, lepton number violation detection in hadron colliders implies tagging two leptons of the same sign in the final state, together with a higher number of jets, making the signal more challenging to search for. In Ref. [10] the process \( pp \to l^+l^+jjjj \) is studied with the same effective formalism we apply here, and the authors claim that it is possible to expect a 5\(\sigma\) same-sign lepton signal for \( m_N \leq 600\text{GeV} \). As will be shown, we expect a significant signal for larger masses, in particular, for \( E_e \leq 50\text{GeV} \) we expect \( m_N \lesssim 700\text{GeV} \), and for \( E_e \leq 150\text{GeV} \), we expect \( m_N \lesssim 1300\text{GeV} \). The ATLAS collaboration has published new physics searches in the same-sign dilepton signal for this model [29, 30], finding limits for the Majorana neutrino mass and certain effective couplings.

In Sec. II we review the effective Lagrangian approach and present our results for the scattering amplitudes. The numerical results are presented in Sec. III, including the SM backgrounds, the neutrinoless double-\(\beta\) decay bounds considered, and the obtained cross sections and discovery regions for the Majorana neutrino. Our conclusions are presented in Sec. IV.

II. EFFECTIVE LAGRANGIAN AND SCATTERING AMPLITUDES

The effects of new physics beyond the SM can be parametrized by a series of effective operators \( \mathcal{O} \) constructed with the SM and the Majorana neutrino fields and preserving the \( SU(2)_L \otimes U(1)_Y \) gauge symmetry [31, 32]. These effective operators represent the low-energy limit of an unknown theory, and their effects are suppressed by inverse powers of the new physics scale \( \Lambda \). We consider the lowest-order new physics terms, taking into account only dimension-6 operators and nonviolating baryon number interactions and discarding the operators generated at one-loop level in the underlying full theory, as they are naturally suppressed by a \( \mathcal{O} \sim 1/16\pi^2 \) factor [10, 33].
The total Lagrangian is organized as:

\[ \mathcal{L} = \mathcal{L}_{SM} + \sum_{J,i} \frac{\alpha^{(i)}_{J}}{\Lambda^{2}} \mathcal{O}^{i}_{J} \]  

where the indices \( J \) and \( i \) label the operators and families respectively. For the considered operators we follow Ref.\[10\] starting with a rather general effective Lagrangian density for the interaction of a Majorana neutrino \( N \) with leptons and quarks. All the operators listed here are generated at tree level in the unknown fundamental high-energy theory. The operators involving scalars and vectors are

\[ \mathcal{O}^{i}_{LN\phi} = (\phi^\dagger \phi)(\bar{L}_{i}N\phi), \quad \mathcal{O}^{i}_{NN\phi} = i(\phi^\dagger D_{\mu}\phi)(\bar{N}\gamma^{\mu}N), \quad \mathcal{O}^{i}_{Ne\phi} = i(\phi^{T} \epsilon D_{\mu}\phi)(\bar{N}\gamma^{\mu}e_{i}) \]  

and for the baryon-number conserving 4-fermion contact terms, we have

\[ \mathcal{O}^{i}_{d_uNe} = (\bar{d}_{i}\gamma^{\mu}u_{i})(\bar{N}\gamma_{\mu}e_{i}), \quad \mathcal{O}^{i}_{fNN} = (\bar{f}_{i}\gamma^{\mu}f_{i})(\bar{N}\gamma^{\mu}N), \]  

\[ \mathcal{O}^{i}_{Q_uNL} = (\bar{Q}_{i}u_{i})(\bar{N}L_{i}), \quad \mathcal{O}^{i}_{Q_NLd} = (\bar{Q}_{i}N)(\bar{L}_{i}d_{i}), \]  

\[ \mathcal{O}^{i}_{LN} = |\bar{L}_{i}N|^2 \]  

where \( e_{i}, u_{i}, d_{i} \) and \( L_{i}, Q_{i} \) denote the \( SU(2) \) right-handed singlets and left-handed doublets, respectively. These are the contributing operators to the Majorana neutrino \( N \) production and decay processes.

The relevant effective Lagrangian terms contributing to the production process considered are:

\[ \mathcal{L}_{eff}^{N} = \frac{1}{\Lambda^{2}} \left\{ -\frac{m_{W}v}{\sqrt{2}} \alpha^{(i)}_{W} W^{\dagger}_{\mu} N R_{\gamma^{\mu}}e_{R,i} + \alpha^{(i)}_{V_{0}} \bar{d}_{R,i}\gamma^{\mu}u_{R,i}\bar{N} R_{\gamma^{\mu}}e_{R,i} + \alpha_{S_{1}}^{(i)}(\bar{u}_{L,i}u_{R,i}\bar{N} \nu_{L,i} - \bar{d}_{L,i}d_{R,i}\bar{N} \epsilon_{L,i}) + \alpha_{S_{2}}^{(i)}(\bar{\nu}_{L,i}N_{R}\bar{d}_{L,i}d_{R,i} - \bar{e}_{L,i}N_{R}\bar{u}_{L,i}d_{R,i}) + \alpha_{S_{3}}^{(i)}(\bar{u}_{L,i}N_{R}\bar{e}_{L,i}d_{R,i} - \bar{d}_{L,i}N_{R}\bar{\nu}_{L,i}d_{R,i}) + h.c. \right\} \]  

where the sum over \( i \) is understood and the constants \( \alpha^{(i)}_{J} \) are associated to specific operators

\[ \alpha^{(i)}_{W} = \alpha^{(i)}_{Ne\phi}, \quad \alpha^{(i)}_{V_{0}} = \alpha^{(i)}_{d_uNe}, \quad \alpha^{(i)}_{S_{1}} = \alpha^{(i)}_{QuNL}, \quad \alpha^{(i)}_{S_{2}} = \alpha^{(i)}_{LNQd}, \quad \alpha^{(i)}_{S_{3}} = \alpha^{(i)}_{Q_NLd}. \]  

Using the effective Lagrangian in Eq.(10), we calculate the cross section for the production of the Majorana neutrino according to the processes shown in Fig.(1). Taking the center of
FIG. 1: Diagrams contributing to the production of Majorana neutrinos in $ep$ colliders.

Mass energy $\sqrt{s} = \sqrt{4E_eE_p}$, $\hat{\sigma}$ and $\hat{s}$ to be the parton level scattering cross section, and the squared center-of-mass energy, and with $x$ the usual deep inelastic scaling variable, we obtain

$$\sigma(ep \to l^+ + 3\text{jets}) = \sum_i \int \frac{1}{m_N^2/s} dx f_i(x) \hat{\sigma}_i(xs)$$

where $i = 1$ corresponds to the channel $eu \to N\bar{d}$ and $i = 2$ corresponds to the crossed channel $e\bar{u} \to N\bar{u}$ obtained by the crossing symmetry. The function $f_1(x)$ represents the $u(x)$ parton distribution function (PDF), and $f_2(x)$ represents the one for $\bar{d}(x)$ and

$$\hat{\sigma}_i(xs) = \int (2\pi)^4\delta^{(4)}(p_e + p_u - \sum_{j=1,4} k_j)|M(i)|^2 \prod_{j=1,4} \frac{d^4k_j}{2\pi^3}.$$ (13)

The squared scattering amplitudes in the narrow width aproximation are

$$|M_{(i)}|^2 = \left(\frac{\pi}{4m_N \Gamma_N \hat{s}}\right) \delta(k_N^2 - m_N^2)|\Lambda_{(i)}|^2 (|\Lambda_{(i)}^{(+)}|^2 + |\Lambda_{(i)}^{(-)}|^2)$$ (14)
where

\[
|\Lambda^{(1)}_{(1)}|^2 = \frac{4}{\Lambda^2} \left[ (\alpha_{S_3} (\alpha_{S_2} - \alpha_{S_3}) + \alpha_{S_3}^2)(k_d \cdot p_u)(k_N \cdot p_e) + 
(4\alpha_W^2 |\Pi^{(2)}_W|^2 + \alpha_{S_3} (\alpha_{S_3} - \alpha_{S_2})) (k_d \cdot p_e) (k_N \cdot p_u) + (\alpha_{S_3} \alpha_{S_2} + 4\alpha_{V_0}^2)(k_d \cdot k_N) (p_e \cdot p_u) \right]
\]

\[
|\Lambda^{(-)}_{(II)}|^2 = \frac{16}{\Lambda^4} \left[ |\Pi^{(2)}_W|^2 \alpha_{S_3}^2 (k_N \cdot l_u)(k_{l+} \cdot l_d) + \alpha_{V_0}^2 (k_N \cdot l_d)(k_{l+} \cdot l_u) \right]
\]

\[
|\Lambda^{(+)}_{(II)}|^2 = \frac{4}{\Lambda^4} \left[ (\alpha_{S_3}^2 + \alpha_{S_2}^2 - \alpha_{S_2} \alpha_{S_3})(l_u \cdot l_d)(k_{l+} \cdot k_N) + 
(\alpha_{S_3}^2 - \alpha_{S_2} \alpha_{S_3})(k_{l+} \cdot l_d)(l_u \cdot k_N) + \alpha_{S_2} \alpha_{S_3}(l_u \cdot k_{l+})(l_d \cdot k_N) \right]
\]

(15)

with \(\Pi^{(1)}_W = m_W^2/(-2(p_u \cdot k_d) - m_W^2)\), \(\Pi^{(2)}_W = m_W^2/(2(l_u \cdot l_d) - m_W^2)\). The final leptons can be either of \(e^+, \mu^+\) or \(\tau^+\) since this is allowed by the interaction Lagrangian (Eq. (10)). All these possible final states are clear signals for intermediary Majorana neutrinos, and thus we sum the cross section over the flavors of the final leptons. The total width \(\Gamma_N\) for the Majorana neutrino decay is calculated in Ref. [21].

### III. NUMERICAL RESULTS

For the numerical study we assume an LHC-like beam of protons with an energy of 7 TeV, while examining two choices for the electron beam. We consider a low-energy scenario with an electron beam of \(E_e = 50\) GeV (Scenario 1), and another high-energy scenario with \(E_e = 150\) GeV (Scenario 2). For each experimental setup we assume a baseline integrated luminosity of \(L = 100\) fb\(^{-1}\) that is close to the values discussed for the LHeC proposal [4].

The branching ratios, cross sections and discovery regions for the Majorana neutrino in the effective Lagrangian approach considered in this paper depend on the quotient of the coupling constant \(\alpha_{J}^{(i)}\), associated with the operators in Eq. (10), and the new physics scale \(\Lambda^2\) squared i.e. \(\kappa_{J}^{(i)} = \alpha_{J}^{(i)}/\Lambda^2\), in addition to the Majorana neutrino mass \(m_N\). The considered operators are bounded by LEP and low-energy data and we have also taken into account the bounds on the operators that come from the neutrinoless double-\(\beta\) decay (0\(\nu\)\(\beta\beta\)-decay).

We start this section discussing the SM backgrounds, the LEP, low-energy data and 0\(\nu\)\(\beta\beta\)-decay bounds, before showing our results for the scattering cross section for the process \(e^-p \rightarrow l_j^+ + 3\)jets, the different distributions and cuts implemented, and the Majorana neutrino discovery regions for both considered scenarios.
A. Standard Model background

The considered signal, being a lepton number violating process, is strictly forbidden in the Standard Model. The SM background will always involve additional light neutrinos that escape the detectors and generate missing energy. This fact makes the signal very clean and difficult to mimic by SM processes.

As was pointed out in Ref.[27], the dominant background comes from $W$ production, with its subsequent decay into $l^+ (e^+, \mu^+, \tau^+)$. In particular, the process $e^- p \rightarrow e^- l^+ jj j \nu$ is not distinguished from the signal if the outgoing electron is lost in the beam line. This process is dominated by the exchange of an almost real photon with a very collinear outgoing electron ($p \gamma \rightarrow l^+ jj j \nu$). This last process, convoluted with the PDF representing the probability of finding a photon inside an electron, is found to be the major contribution to $W$ production.

The simulation of the background processes was done using the program CalcHep [34]. In Sect. [III] we discuss different cuts to increase the sensitivity and improve the signal-to-background relation.

B. LEP, low-energy, and neutrinoless double-$\beta$ decay bounds

The heavy Majorana neutrino couples to the three flavor families with couplings $\kappa^{(i)} = \alpha^{(i)} / \Lambda^2$. These couplings can be related with the mixing angle between light and heavy neutrinos $U_{lN}$, comparing the operator $\mathcal{O}^{(i)}_{N_{e\phi}}$ with the strength of the vector-axial vector interaction in Eq.[3]. The relation is $U_{lN} = \frac{\nu^2 \alpha^{(i)} }{2 \Lambda}$. The mixing angles $U_{lN}$ are bounded by LEP and low-energy data [35–40]. In our case, with only one heavy neutrino $N$, and following the treatment made in Refs. [21, 35], we translate these model-independent bounds to the couplings $\kappa^{(i)}$, considering that all the operators satisfy the same and most stringent constraint given on Ref. [40] for $\Omega_{e\mu} = U_{eN} U_{\mu N} = \frac{\nu^2}{2} \kappa^2 < 1.0 \times 10^{-4}$ with $\nu = 250$ GeV. This leads to $\kappa < 3.2 \times 10^{-7}$ GeV$^{-2}$, which, as we will show, is less restrictive than the the constraints imposed by the $0\nu\beta\beta$-decay experiments.

To take into account the constraints imposed by the $0\nu\beta\beta$-decay experiments on some of the coupling constants $\alpha^{(i)}$, we follow the developments presented in Refs.[41, 42] and take the most stringent limits on the lifetime for neutrinoless double-$\beta$ decay ($\tau_{0\nu\beta\beta} \geq 2.1 \times 10^{25}$ yr) obtained by the GERDA collaboration [43].
FIG. 2: Contribution to $0\nu\beta\beta$-decay. In the diagram (a), the solid dot represents the operator $\mathcal{O}_{Ne\phi}^1$ and in the diagram (b) the dot represents the 4-fermion operators $\mathcal{O}_{duNe}^1$, $\mathcal{O}_{QuNL}^1$, $\mathcal{O}_{LNQd}^1$ and $\mathcal{O}_{QNLd}^1$.

The lowest-order contribution to $0\nu\beta\beta$-decay from the considered effective operators comes from those that involve the $W$ field and the 4-fermion operators with quarks $u, d$, the lepton $e$ and the Majorana neutrino $N$:

\[
\mathcal{O}_{Ne\phi}^1, \mathcal{O}_{duNe}^1, \mathcal{O}_{QuNL}^1, \mathcal{O}_{LNQd}^1, \mathcal{O}_{QNLd}^1.
\]  

(16)

The contribution of these operators to $0\nu\beta\beta$-decay is shown in Fig. 2.

For the coupling constant associated with each operator we use the generic name $\alpha_{0\nu\beta\beta}$; that is to say

\[
\alpha_{0\nu\beta\beta} = \alpha_{Ne\phi}^{(1)} = \alpha_{duNe}^{(1)} = \alpha_{QuNL}^{(1)} = \alpha_{LNQd}^{(1)} = \alpha_{QNLd}^{(1)}.
\]  

(17)

To estimate the bounds on the different $\alpha_{j}^{(i)}$ we consider the case in which all coupling constants $\alpha$ are nonzero with equal values, and the individual contributions of each operator are considered to act alone. The maximum value for the $\alpha$'s is limited by the $0\nu\beta\beta$ bound.

Following the treatment made in Ref. [21], we obtain the bound value for the quotient

\[
\kappa_{0\nu\beta\beta} = \frac{\alpha_{0\nu\beta\beta}}{\Lambda^2} \leq 7.8 \times 10^{-8}\left(\frac{m_N}{100 \text{GeV}}\right)^{1/2}
\]  

(18)
C. Signal cross section

We have already discussed in the previous section that some of the operators that contribute to the neutrinoless double beta decay ($0\nu\beta\beta$-decay) may be strongly constrained. Therefore, for studying the Majorana neutrino production cross section in $ep$ colliders and the following decay $N \rightarrow l^+ + 2jets$ we analyze two situations: in Set I we consider the case in which the effective couplings for the operators that do not contribute to neutrinoless decay take all the same value $\alpha = 1$, and in Set II we consider all those effective couplings to be equal and limited by the neutrinoless double beta decay bound Eq.(18).

The Majorana neutrino width was studied in detail in Ref.[21], in which all possible effective operators of dimension-6 involving quarks were taken into account.

In Fig.3a we show the results for the cross section, as a function of the Majorana neutrino mass $m_N$, for the considered electron beam energies: $E_e = 50$ GeV (Scenario 1) and $E_e = 150$ GeV (Scenario 2) for both Sets I and II. The results are very similar for both sets. We have considered $\sqrt{s} < \Lambda$ in order to ensure the validity of the effective Lagrangian approach. We display here the results for $\Lambda = 2500$ GeV.

![Signal cross section](image1.png)

(a) Signal cross section.

![Background $E_T$ dependence](image2.png)

(b) Background $E_T$ dependence.

FIG. 3: Cross section for the process $ep \rightarrow NX$ with $N$ decaying according to Ref.[21] (a) and background dependence with missing $E_T$ (b).

The phase-space integration of the squared amplitude is made generating the final momenta with the Monte Carlo routine RAMBO [44]. This allows us to make the distributions and necessary cuts in the phase space to study the possibility of discovering Majorana neu-
trino effects.

D. Distributions and kinematical cuts.

The dominant backgrounds for the studied process have been analyzed in Ref. [27]. In particular, the authors conclude that a cut that could be effective to separate the signal and background is to reject events in which the outgoing $l^+$ does not have a minimum transverse momentum. On the other hand, as the signal only includes visible particles and the background includes at least one neutrino, another possible cut is imposing an upper bound on the missing transverse energy. We follow this approach and implement the mentioned cuts. In Fig. 3b we show the behavior of the background with the maximum missing energy $E_T$ for the scenarios in which $E_e = 50$ GeV (Scenario 1) and $E_e = 150$ GeV (Scenario 2). A cut of $E_{T,max} \leq 10$ GeV, which is a reasonable value for the detector resolution, does not have appreciable effects on the signal but reduces the background significantly. In Fig. 4 we show the differential cross section for the background and the signal for different values of the Majorana mass as a function of the transverse momentum $p_{T,l^+}$ of the antilepton. In these figures the cut on the missing energy $E_T$ has already been included. As it can be appreciated, the background is mostly concentrated at low values of $p_{T,l^+}$, and a cut imposed on $p_{T,l^+}^{min}$ could be effective to improve the signal/background relation. Finally, in Fig. 5 we show a plot comparing the magnitude of the signal for different values of the Majorana neutrino mass (solid lines), and the background for different $E_{T,max}$ cuts (dashed lines), depending on the $p_{T,l^+}^{min}$ cut imposed. In both figures the arrows indicate the value of the cuts used in the analysis: we impose $p_{T,l^+} \geq 90$ GeV and $E_{T,miss} \leq 10$ GeV in order to reduce the background without appreciably decreasing the signal.

E. Discovery regions

To investigate the possibility of the detection of Majorana neutrinos in the process under consideration, we study the region (discovery region) where the signal can be separated from the background with a statistical significance higher than $5\sigma$. We use the method of the effective significance described in Refs. [45, 46]. There they show that the effective
FIG. 4: Differential cross section of signal and background in function of transverse momentum $p_{T,l^+}$. The cut in missing $E_T$ is included.

FIG. 5: Comparison between signal and background for different Majorana neutrino masses, cut in missing $E_T$ and the transversal momentum of the final lepton $p_{T,l^+}$. The solid lines show the cross section for the signal, and the dotted lines, show the cross section for the background. The arrows indicate the cuts and backgrounds used in the analysis.

significance is well approximated by

$$S = 2\left(\sqrt{n_s} + \sqrt{n_b} - \sqrt{n_b}\right) - k(\alpha)$$

with $k(\alpha) = 1.28$ for $\alpha = 0.1$ where $1 - \alpha$ is the probability of measuring a number of events bigger than a value $n_0$, such that the probability ($\beta$) that the Standard Model reproduces
such number is rather small, \( \beta < 3 \times 10^{-7} \) for \( S > 5 \) (5\( \sigma \) test). In Eq. (19) \( n_s = L\sigma_s \) and \( n_b = L\sigma_b \) are the numbers of events for the signal and backgrounds, with \( L \) being the luminosity.

In Fig. 6 we show the discovery regions for different values of the Majorana neutrino mass \( m_N \), and the quotient \( \kappa_{J}^{(i)} = \frac{\alpha_{J}^{(i)}}{\Lambda^2} \). As we explained in Sec. IIIB, we consider the case in which all the 0\( \nu \)\( \beta \beta \) contributing coupling constants \( \alpha_J^{(i)} \) (generically \( \alpha \)) are nonzero and equal, so that \( \kappa \leq \kappa_{0\nu\beta\beta} \) in Eq. (18). The figure shows that Majorana neutrinos of masses up to near 1300 GeV for Scenario 1, and 700 GeV for Scenario 2 may be detected.

**FIG. 6:** Majorana neutrino discovery regions at 5\( \sigma \). The horizontal line represents the low-energy and LEP limits discussed in Sec. IIIB.

The maximum allowed value for the Majorana neutrino mass corresponds to the intersection between the 0\( \nu \)\( \beta \beta \) bound Eq. (18) and the contour of level 5 for the surface \( S \) Eq. (19); this is: \( S(m_N, \Lambda) = 5 \). The last equation can be written as \( \alpha_{0\nu\beta\beta}/\Lambda^2 \approx f(m_N) \) where \( f \) is a function of \( m_N \) and the collider energy but independent of \( \Lambda \). Thus, the intersection and then the maximum possible value for \( m_N \) is almost independent of the new physics scale \( \Lambda \).

Systematic uncertainties are hard to estimate without a detailed reconstruction of the detector, but they are expected to be around a few percent [47]. However, the influence of the background systematic uncertainties in the result is small because the background itself is small. In the case of the signal we have calculated the modifications for the discovery
region if the number of events for the signal is changed by ±30%. The results are shown in Fig. 7 showing no appreciable change in the region.

IV. SUMMARY AND CONCLUSIONS

To investigate the possibilities for discovering Majorana neutrinos in an $e^-p$ collider at CERN (LHeC), we have calculated the cross section for the lepton number violating process $e^-p \rightarrow l^+_j + 3jets$ in an effective Lagrangian approach, complementing previous analyses for this facility involving typical seesaw scenarios.

The effective Lagrangian framework parameterizes new physics effects in a model independent way, allowing for sizable lepton number violating effects for effective couplings $\alpha^{(i)}_{\mathcal{J}}$ of order 1, in contrast to the minimal seesaw mechanism, that leads to the decoupling of the Majorana neutrinos.

While models like the minimal seesaw mechanism lead to the decoupling of the heavy Majorana neutrinos, predicting unobservable LNV, the effective Lagrangian framework considered in this work parameterizes the new physics effects in a model-independent way, enabling the occurrence of sizable LNV signals for effective couplings $\alpha^{(i)}_{\mathcal{J}}$ of order 1.

We have calculated the total unpolarized cross section $\sigma(e^-p \rightarrow l^+_j + 3jets)$ for different
values of $m_N$, the effective couplings $\alpha^{(i)}_J$ and the new physics scale $\Lambda$, and implemented cuts in the phase space that can help to enhance the signal-to-background relation. We obtained the Majorana neutrino discovery regions at $5\sigma$ statistical significance, combining the effect of the SM backgrounds with the most restrictive $0\nu\beta\beta$-decay bounds for the effective couplings.

Our analysis shows that the LHeC facility could discover Majorana neutrinos with masses lower than 700 and 1300 GeV with a 7 TeV proton beam, and electron beams of $E_e = 50$ and $E_e = 150$ GeV respectively. Thus, we find lepton-proton colliders could provide a new probe of the Majorana nature of neutrinos, shedding light on this fundamental unsolved issue in particle physics.

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