Electroweak Sector Under Scrutiny: A Combined Analysis of LHC and Electroweak Precision Data

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We perform a comprehensive study of the Higgs couplings, gauge-boson couplings to fermions and triple gauge boson vertices. We work in the framework of effective theories including the effects of the dimension-six operators contributing to these observables. We determine the presently allowed range for the coefficients of these operators via a 20 parameter global fit to the electroweak precision data, as well as electroweak diboson and Higgs production data from LHC Run 1 and 2. We quantify the improvement on the determination of the 20 Wilson coefficients by the inclusion of the Run 2 results. In particular we present a novel analysis of the ATLAS Run 2 36.1 fb$^{-1}$ data on the transverse mass distribution of $W^+W^-$ and $W^\pm Z$ in the leptonic channel which allow for stronger tests of the triple gauge boson vertices. We discuss the discrete (quasi)-degeneracies existing in the parameter space of operator coefficients relevant for the Higgs couplings to fermions and gauge bosons. In particular we show how the inclusion of the incipient $tH$ data can break those degeneracies in the determination of the top-Higgs coupling. We also discuss and quantify the effect of keeping the terms quadratic in the Wilson coefficients in the analysis and we show the importance of the Higgs data to constrain some of the operators that modify the triple gauge boson couplings in the linear regime.

I. INTRODUCTION

Since the discovery of a new state resembling the SM Higgs boson \cite{Aad:2012tfa,Khachatryan:2014jba}, the CERN Large Hadron Collider (LHC) has accumulated an impressive amount of data that allow new searches for extensions of the Standard Model (SM), as well as detailed studies of the SM predictions. Presently, the negative results of the search for direct new physics effects indicate that new states are probably heavy, therefore, there might exist a mass gap between the SM states and the new ones. In this scenario, hints on the new physics can manifest itself first through deviations from the SM predictions.

Against this background, effective lagrangians raise as a most adequate tool for scientific advancement. The effective lagrangian approach \cite{Weinberg:1979sa,Georgi:1984af} is a model–independent framework, which, using as inputs the low energy particle contents and symmetries, describes new physics that is expected to manifest itself directly at an energy scale $\Lambda$ larger than the scale at which the experiments are performed, by including in the lagrangian higher–dimension operators. In this context, and within the present experimental results, we proceed by assuming that the observed scalar belongs indeed to a light electroweak doublet and that the $SU(2)_L \otimes U(1)_Y$ symmetry is linearly realized in the effective theory.
Barring effects associated with violation of total lepton number, the lowest order operators which can be built are of dimension six. The coefficients of these dimension–six operators parametrize our ignorance of the new physics effects and our task at hand is to determine them using the available data.

In this work we follow this road by performing a comprehensive analysis of the observables related to the electroweak sector, which at present allows for precision tests of the couplings between electroweak gauge bosons and fermions, triple electroweak gauge couplings (TGC) and the couplings of the Higgs to fermions and gauge bosons. The first two sets of couplings allow us to probe the $SU(2)_L \otimes U(1)_Y$ gauge structure of the SM, while the last one aims the study of the couplings of the recently discovered scalar, i.e. to directly probe the electroweak symmetry breaking mechanism. In this respect, this work extends and updates our previous partial constrains on Higgs anomalous couplings and TGC’s [6–9].

In the framework of the effective lagrangian described above (also lately labeled in the literature as the SMEFT) our study involves twenty dimension–six operators whose coefficients are determined by means of a global fit to the relevant data, including low energy electroweak precision measurements as well as LHC data on gauge boson pair production and Higgs observables. The global analysis approach (see Ref. [10][11] for recent related works) is becoming mandatory because within the present LHC statistics, changes in the couplings of gauge bosons to fermions, even within the constraints of electroweak precision data (EWPD) can lead to modifications of the kinematical distributions in gauge boson pair production at LHC of comparable size to the ones stemming from the purely anomalous TGC [12–14]. And these, in turn, influence the determination of the Wilson coefficients for the operators entering the Higgs observables.

With this aim we briefly introduce in Sec. II the set of dimension–six operators included in our study and point out the main sources of (quasi)-degenerate solutions which appear in the analysis. Section III contains a brief description of the data and statistical treatment applied to it. For the Higgs observables this includes the final results of the LHC Run 1 and the most up to date from Run 2 in terms of signal strengths or ratios of cross sections and branching ratios. Concerning the gauge boson pair production data, besides the final results of the LHC Run 1, we perform a novel analysis of the ATLAS data on transverse mass distribution of $W^+W^-$ and $W^\pm Z$ in the leptonic channel. The body of ours results are discussed in Sec. IV which we present in terms of the different sectors tested: gauge-boson-fermion couplings, TGC’s and Higgs couplings. One particularly interesting observation is the relevance of the incipient $tH$ data to break possible degeneracies in the determination of the top Yukawa coupling. We finish Sec. IV with a quantification of the relevance of keeping the terms quadratic in the Wilson coefficients in the analysis. In that respect our results show that the accumulated statistics on the Higgs observables is starting to be large enough for meaningful constraints on the Wilson coefficients of some of the operators to be imposed from their interference with the SM contributions. We summarize our findings in Sec. V.

II. THEORETICAL FRAMEWORK

Up to now there is no direct evidence of new states being produced at the LHC. Therefore, we parametrize possible deviations from the SM by higher-dimension operators:

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_{n \geq 4, j} \frac{f_{n,j}}{\Lambda^{n-4}} O_{n,j},$$

(2.1)

where the SM $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$ gauge symmetry is realized linearly in the $O_{n,j}$ operators. For the sake of simplicity we retain only the dimension–six operators that conserve $C$, $P$ and lepton and baryon numbers. The first higher-order operator is of dimension five [15], however, it does not contribute to the LHC physics due to the strong constraints originating from the neutrino sector. The first operators to play a significant role at the LHC are of dimension six, i.e. $n = 6$. It is well known that there are 59 independent dimension–six operators [16], up to flavor and hermitian conjugation. Using the freedom in the choice of basis [17][20] due to the use of equations of motion (EOM), we work in that of Hagiwara, Ishihara, Szalapski, and Zeppenfeld (HISZ) [21][22] for the pure bosonic operators.
In what follows we focus on the subset of the dimension–six operator basis that impact the precision electroweak data (EWPD) \cite{23}, TGC’s, and Higgs physics. The EWPD observables receive linear contributions from seven operators involving fermions, gauge bosons and the Higgs field:

\begin{align}
\mathcal{O}_{\Phi L,ij}^{(1)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{L}_i \gamma^\mu L_j), & \mathcal{O}_{\Phi L,ij}^{(2)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{L}_i \gamma^\mu T_a L_j), \\
\mathcal{O}_{\Phi Q,ij}^{(1)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{Q}_i \gamma^\mu Q_j), & \mathcal{O}_{\Phi Q,ij}^{(2)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{Q}_i \gamma^\mu T_a Q_j), \\
\mathcal{O}_{\Phi u,ij}^{(1)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{u}_R \gamma^\mu u_R), & \mathcal{O}_{\Phi d,ij}^{(1)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{d}_R \gamma^\mu d_R), \\
\mathcal{O}_{\Phi e,ij}^{(1)} &= \Phi^\dagger (iD^\mu \Phi)(\bar{e}_R \gamma^\mu e_R),
\end{align}

(2.2)

together with a purely four fermion operator:

\[ \mathcal{O}_{LLLL} = (\bar{L} \gamma^\mu L)(\bar{L} \gamma^\mu L). \]  

(2.3)

In addition to the above fermionic operators there are two bosonic operators that contribute to the EWPD

\[ \mathcal{O}_{BW} = \Phi^\dagger \hat{B}_{\mu\nu} \hat{W}^{\mu\nu} \Phi \quad \text{and} \quad \mathcal{O}_{\Phi,1} = (D^\mu \Phi)^\dagger \Phi^\dagger (D^\nu \Phi). \]  

(2.4)

In the equations above \( \Phi \) stands for the SM Higgs doublet while lepton (quark) doublet is denoted by \( L \) (\( Q \)) and \( f_R \) are the \( SU(2)_L \) singlet fermions, where \( i, j \) are family indices. In addition, we defined \( \Phi^\dagger D^\mu \Phi = \Phi^\dagger D^\mu \Phi - (D^\mu \Phi)^\dagger \Phi \) and \( \Phi^\dagger D^\mu D^\nu \Phi = \Phi^\dagger T^a D^\mu \Phi - (D^\mu \Phi)^\dagger T^a \Phi \) with \( T^a = \sigma^a / 2 \). Also, we defined \( \hat{B}_{\mu\nu} \equiv i(g'/2)B_{\mu\nu} \) and \( \hat{W}_{\mu\nu} \equiv i(g/2)\sigma^a W^a_{\mu\nu} \), with \( g \) and \( g' \) being the \( SU(2)_L \) and \( U(1)_Y \) gauge couplings respectively. The Pauli matrices are denoted by \( \sigma^a \).

The seven operators in Eq. \((2.2)\) modify directly the coupling of the \( Z \) to fermion pairs while \( \mathcal{O}_{\Phi Q,ij}^{(3)} \) contributes also to the \( W \) couplings to left quarks. \( \mathcal{O}_{LLLL} \), \( \mathcal{O}_{BW} \) and \( \mathcal{O}_{\Phi,1} \) contributions are ubiquitous and stem from their effect on the finite renormalization of the SM fields and couplings once the lagrangian is canonically normalized. In particular \( \mathcal{O}_{LLLL} \) gives a finite contribution to the Fermi constant while the operators \( \mathcal{O}_{BW} \), and \( \mathcal{O}_{\Phi,1} \) lead to finite correction to the \( S \) and \( T \) oblique parameters respectively. Furthermore, in the analysis of EWPD we did not considered six dipole operators whose interference with the SM contributions vanish for EWPD observables.

In what follows, in order to avoid the existence of blind directions \cite{24, 25} in the EWPD analyses, we used the freedom associated to the use of EOM to remove the operator combinations

\[ \sum_i \mathcal{O}_{\Phi L,ii}^{(1)} \quad \text{and} \quad \sum_i \mathcal{O}_{\Phi L,ii}^{(3)} \]  

(2.5)

from our operator basis. Moreover, we assume no family mixing in the above operators to prevent the generation of too large flavor violation and for simplicity we consider the operators to be generation independent; hereafter, we drop the generation indexes for these operators. With these hypothesis, the operators \( \mathcal{O}_{\Phi L}^{(1)} \) and \( \mathcal{O}_{\Phi L}^{(3)} \) are removed by the use of EOM \cite{7}.

With the above assumptions, in our basis, only the operator \( \mathcal{O}_{\Phi c}^{(1)} \) modifies the \( Z \) coupling to leptons, while there are additional contributions to the \( Z \)-quark pair vertices originating from \( \mathcal{O}_{\Phi u}^{(1)}, \mathcal{O}_{\Phi d}^{(1)}, \mathcal{O}_{\Phi Q}^{(1)} \), and \( \mathcal{O}_{\Phi Q}^{(3)} \). Moreover, the \( W \) coupling to fermions receives extra contributions from \( \mathcal{O}_{\Phi Q}^{(3)} \); see Table 1.

Altogether the part of the dimension–six effective lagrangian that contributes to the EWPD is

\[ \Delta \mathcal{L}_{\text{eff}}^{\text{EWPD}} = \frac{f_{\Phi Q}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi Q}^{(1)} + \frac{f_{\Phi Q}^{(3)}}{\Lambda^2} \mathcal{O}_{\Phi Q}^{(3)} + \frac{f_{\Phi u}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi u}^{(1)} + \frac{f_{\Phi d}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi d}^{(1)} + \frac{f_{\Phi u}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi u}^{(1)} + \frac{f_{\Phi d}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi d}^{(1)} + \frac{f_{\Phi e}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi e}^{(1)} + \frac{f_{BW}}{\Lambda^2} \mathcal{O}_{BW} + \frac{f_{\Phi,1}}{\Lambda^2} \mathcal{O}_{\Phi,1} + \frac{f_{LLLL}}{\Lambda^2} \mathcal{O}_{LLLL}. \]  

(2.6)

As is well known, the above operators are strongly constrained by the EWPD observables \cite{20}.
with the effective lagrangian

\[ \mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{dimension-six}} + \mathcal{L}_{\text{vector}}. \]

Finally the couplings of the Higgs to gauge bosons are further modified by the bosonic operators

\[ \mathcal{O}_{\mathcal{G}G} = \Phi^1 \Phi G_{\mu\nu} \hat{G}^{\mu\nu} + \mathcal{O}_{\mathcal{W}W} = \Phi^1 \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \Phi, \]

\[ \mathcal{O}_{\mathcal{B}B} = \Phi^1 \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \Phi, \]

\[ \mathcal{O}_{\Phi, 22} = \frac{1}{2} \partial_\mu (\Phi^1 \Phi) \partial_\mu (\Phi^1 \Phi). \]

Data on electroweak diboson production processes (here on EWDBD) at the LHC, \( pp \rightarrow W^+W^- \) and \( pp \rightarrow ZW^{\pm} \), can be used to study operators that change the \( W \) and \( Z \) couplings to fermions, as well as TGC. These processes receive contributions from the previously discussed operators, as well as from the fermionic operator

\[ \mathcal{O}_{\Phi, ud}^{(1)} = \Phi^1 (i \hat{D}_{\mu} \Phi) (\bar{u}_R)^\mu d_R + \text{h.c.}, \]

that modifies the couplings of \( W \)’s to right-handed quark pairs and does not interfere with the SM contributions to the EWPD observables at the order considered in the analysis. In addition, TGC’s are also modified by two additional dimension–six operators that include Higgs and electroweak gauge fields in the HISZ basis

\[ \mathcal{O}_W = (D_\mu \Phi)^1 \hat{W}_{\mu\nu} (D_\nu \Phi) \quad \text{and} \quad \mathcal{O}_B = (D_\mu \Phi)^1 \hat{B}_{\mu\nu} (D_\nu \Phi), \]

and by one operator that contains exclusively gauge bosons

\[ \mathcal{O}_{WWW} = \text{Tr} [\hat{W}_{\mu} \hat{W}_{\nu} \hat{W}_{\rho}]. \]

We present in Table I the anomalous TGC stemming from the dimension–six operators in our basis. It is interesting to notice that dimension–six operators do not give rise to anomalous TGC among neutral gauge bosons. We define the effective lagrangian of the operators that contribute to TGC in addition to the ones participating in the EWPD analysis as

\[ \Delta \mathcal{L}_{\text{TGC}}^{\text{eff}} = \frac{f_{WWW}}{\Lambda^2} \mathcal{O}_{WWW} + \frac{f_W}{\Lambda^2} \mathcal{O}_W + \frac{f_B}{\Lambda^2} \mathcal{O}_B + \frac{f_{\Phi, ud}^{(1)}}{\Lambda^2} \mathcal{O}_{\Phi, ud}^{(1)} + \text{h.c.}. \]

Concerning Higgs processes, in order to quantify possible deviations from the SM predictions we must consider some additional dimension–six operators that contain the Higgs field \( \Phi \). In particular the following fermionic operators modify the Yukawa couplings of the Higgs boson

\[ \mathcal{O}_{e, ij} = (\Phi^1 \Phi)(L_i \Phi e_{R,j}) \quad \mathcal{O}_{u, ij} = (\Phi^1 \Phi)(\bar{Q}_i \Phi u_{R,j}) \quad \mathcal{O}_{d, ij} = (\Phi^1 \Phi)(\bar{Q}_i \Phi d_{R,j}) \]

with \( \Phi = i \sigma_2 \Phi^* \) and \( i, j \) being generation indices. In this work we consider only the diagonal couplings of Higgs to the third family and also to muon pairs (which are the only ones being currently tested at LHC) – that is, we work with the effective lagrangian

\[ \Delta \mathcal{L}_{\text{eff}}^{\text{Yuk}} = \frac{f_m}{\Lambda^2} \mathcal{O}_{e, 22} + \frac{f_m}{\Lambda^2} \mathcal{O}_{e, 33} + \frac{f_m}{\Lambda^2} \mathcal{O}_{d, 33} + \frac{f_m}{\Lambda^2} \mathcal{O}_{u, 33} + \text{h.c.}. \]

Finally we consider the couplings of the Higgs to gauge bosons which are modified by the bosonic operators

\[ \mathcal{O}_{\mathcal{G}G} = \Phi^1 \Phi G_{\mu\nu} G^{\mu\nu} \quad \mathcal{O}_{\mathcal{W}W} = \Phi^1 \hat{W}_{\mu\nu} \hat{W}^{\mu\nu} \Phi, \]

\[ \mathcal{O}_{\mathcal{B}B} = \Phi^1 \hat{B}_{\mu\nu} \hat{B}^{\mu\nu} \Phi, \quad \mathcal{O}_{\Phi, 22} = \frac{1}{2} \partial_\mu (\Phi^1 \Phi) \partial_\mu (\Phi^1 \Phi). \]
TABLE II: Anomalous couplings of gauge and Higgs bosons induced the dimension–six operators the we consider.

| O_{WW} | γWW | Hγγ | HZZ | HZγ | HWW |
|-------|-----|-----|-----|-----|-----|
| X     | X   | X   | X   | X   | X   |
| O_{W} | X   | X   |     |     |     |
| O_{B} | X   |     |     |     |     |
| O_{BW} | X | X | X | X | X |
| O_{WW} |     | X | X | X | X |
| O_{BB} | X | X | X | | |
| O_{Φ,1} | X |     |     |     |     |
| O_{Φ,2} |     | X |     |     |     |

The operator $O_{Φ,2}$ modifies all Higgs couplings due to a finite renormalization of the Higgs wave function. We keep its effects explicitly in the modification of the Higgs vertices generated from the dimension–four part of the Lagrangian, $L_{SM}$. Corrections to vertices generated by other dimension–six operators are absorbed in the redefinition of the corresponding Wilson coefficient.

As for the effective couplings to gluons, in what follows we work in the convention that the Wilson coefficient of the operator $O_{GG}$ contains not only contributions of new possible colored states appearing in the loop connecting gluon pairs to the Higgs, but also the effects of the anomalous operators that modify the SM Yukawa coupling to bottom and top quarks running in the loop. The effective lagrangian associated to these operators is

$$\Delta L_{HVV}^{eff} = -\frac{\alpha_s}{8\pi} \frac{f_{GG}}{\Lambda^2} O_{GG} + \frac{f_{BB}}{\Lambda^2} O_{BB} + \frac{f_{WW}}{\Lambda^2} O_{WW} + \frac{f_{Φ,2}}{\Lambda^2} O_{Φ,2}.$$  (2.14)

Notice that we rescale the Wilson coefficient $f_{GG}/\Lambda^2$ of the gluon-gluon operator to include a loop suppression factor such that its limits are of the same order of the Wilson coefficients of other operators.

In summary, the total effective lagrangian that we consider is

$$L_{eff} = L_{SM} + \Delta L_{EWPD}^{eff} + \Delta L_{TGC}^{eff} + \Delta L_{Yuk}^{eff} + \Delta L_{HVV}^{eff}.$$  (2.15)

Tables I and II show the anomalous three point vertices generated by the effective lagrangian in Eq. (2.15): the explicit form of the couplings and the different Lorentz structures generated can be found, for example, in Refs. [7, 13, 26, 27] to which we refer the reader for details.

In brief, EWPD constrains at tree level only the eight Wilson coefficients of the operators appearing in $\Delta L_{EWPD}^{eff}$, while the TGC analysis of EWDBD receives contributions from the twelve operators in $\Delta L_{EWPD}^{eff}$ and $\Delta L_{TGC}^{eff}$. On the other hand, nineteen of the twenty operators in $L_{eff}$ are required to study the different Higgs production and decay channels at LHC; in fact, only $O_{WW}$ does not contribute to Higgs processes. Altogether, at dimension six, the global analysis of EWPD, EWDBD and Higgs processes involves the 20 operators in Eq. (2.15).

As we will see in the following section, at present there is enough experimental information to individually bound the 20 Wilson coefficients but there are still important discrete (quasi-)degeneracies. They can be understood in terms of sign flips of the couplings of the Higgs to gauge bosons and to fermions with respect to the SM. For instance, the coefficient of the $HW^+\bar{W}^-\mu$ vertex is

$$\left(\frac{g^2v}{2}\right)\left[1 - \frac{v^2}{4}\left(\frac{f_{Φ,1}}{\Lambda^2} + 2\frac{f_{Φ,2}}{\Lambda^2}\right)\right].$$  (2.16)

Since $f_{Φ,1}/\Lambda^2$ possesses a stringent bound from EWPD, we anticipate a degeneracy with the SM results for $f_{Φ,2}/\Lambda^2 = 0$ and around $f_{Φ,2}/\Lambda^2 = 4/v^2 \sim 65$ TeV$^{-2}$. These points in parameter space are also nearly degenerate for the vertex $HZ_μZ^ν$.

As for the Higgs couplings to fermions, anomalous interactions can also lead to Yukawa couplings of the order of the SM ones but with a different sign as the coefficient of the $H\bar{f}f$ vertex is now

$$-\frac{m_f}{v}\left[1 - \frac{v^2}{2}\left(\frac{f_{Φ,2}}{\Lambda^2} + \sqrt{2}\frac{f_ℓ}{\Lambda^2}\right)\right]$$  (2.17)
constructed a branching ratio for which the average in Ref. [28] is considered. In order to perform the statistical analysis we that are, respectively, its average mass taken from [28], its width from LEP2/Tevatron [29], and the leptonic W pair production at LEP2 [31] and the Run 1 of LHC where the ATLAS and CMS collaborations have used their full details of this part of the statistical analysis we refer the reader to Refs. [14, 26].

The structure of the electroweak triple gauge boson coupling has been the subject of direct scrutiny in gauge boson production but still with data collected with 13.3 fb$^{-1}$ and this data can be used to set better constraints on TGC. With this aim in here we use the ATLAS results on WZ production [39] both with 36.1 fb$^{-1}$ as we describe next.
In order to obtain the bounds on the Wilson coefficients in the effective lagrangian in Eq. (2.15) we study the $W^+W^-$ and $W^\pm Z$ productions in the leptonic channel using the available kinematic distribution that is most sensitive for TGC analysis. More specifically, the channels that we analyze and their kinematical distributions are:

| Channel $(a)$ | Distribution $b$ | # bins | Data set $c$ | Int Lum |
|--------------|------------------|--------|--------------|---------|
| $WW \to \ell^+\ell^- + \not{p_T}^\text{leading,lepton}$ | $p_T^{\ell\ell}$ | 3 | ATLAS $8 \text{ TeV}$, 20.3 fb$^{-1}$ | 32 |
| $WW \to \ell^+\ell^0 + \not{p_T}^\ell (0j)$ | $m_T^{\ell\ell(0)}$ | 8 | CMS $8 \text{ TeV}$, 19.4 fb$^{-1}$ | 33 |
| $WZ \to \ell^+\ell^0 + \not{p_T}^{\ell\ell}$ | $m_T^{WZ}$ | 6 | ATLAS $8 \text{ TeV}$, 20.3 fb$^{-1}$ | 34 |
| $WZ \to \ell^+\ell^- + \not{p_T}^{\ell\ell} (0j)$ | $Z$ candidate $p_T^{\ell\ell}$ | 10 | CMS $8 \text{ TeV}$, 19.6 fb$^{-1}$ | 35 |
| $WW \to e^\pm \mu^\mp + \not{p_T}$ | $m_T$ | 17 | ATLAS $13 \text{ TeV}$, 36.1 fb$^{-1}$ | 39 |
| $WZ \to \ell^+\ell^- (0j)$ | $m_T^{WZ}$ | 6 | ATLAS $13 \text{ TeV}$, 36.1 fb$^{-1}$ | 38 |

For each experiment and channel, we extract from the experimental publications the observed event rates in each bin, $N_i^a$, as well as the background expectations $N_i^{bck}$, and the SM $W^+W^-$ ($W^\pm Z$) predictions, $N_i^{a,sm}$.

For details of the analysis of EWDBD from Run 1 we refer the reader to Ref. [14] that contains our procedure, as well as its validation against the TGC results from the experimental collaborations.

Concerning the Run 2 EWDBD analysis, for the $W^+W^-$ final state we study the transverse mass distribution in the ATLAS $13 \text{ TeV}$ ggF sample. We extract from Fig. 4 in Ref. [39] both the data, the non-WW backgrounds, as well as the SM $WW$ contributions in each of the 17 bins in the transverse mass variable

$$m_T \equiv \sqrt{(E_T^{\ell\ell} + E_T^{\text{miss}})^2 - |p_T^{\ell\ell} + \not{p_T}^{\text{miss}}|^2}$$

(3.2)

with $E_T^{\ell\ell} = \sqrt{|p_T^{\ell\ell}|^2 + m_T^{\ell\ell}^2}$ and the transverse momentum (invariant mass) of the lepton pair denoted by $p_T^{\ell\ell}$ ($m_T^{\ell\ell}$).

The statistical uncertainty is given by $\sqrt{N_i^{WW}}$ where we combine the contents of the last 3 bins to ensure gaussianity. Theoretical and systematic uncertainties can be found in Tables 5-7 of the same reference. For the $13 \text{ TeV}$ $W^\pm Z$ final state, we make the analysis using the transverse mass distribution in Fig. 4c in Ref. [39] which is presented in terms of $W^\pm Z$ signal events in 6 bins covering all values of $m_T^{WZ}$ (last bin containing all data above 600 GeV) and already background subtracted. From the lower panel of the same figure we read the statistical, total experimental and theoretical uncertainties in each bin.

With that information the procedure to obtain the relevant kinematical distributions predicted in presence of the dimension-six operators is the same followed for our Run 1 EWDBD analysis [14]. First we simulate the $W^+W^-$ and $W^\pm Z$ productions using MadGraph5 [40] with the UFO files for our effective lagrangian generated with FeynRules [41, 42]. We employ PYTHIA6.4 [43] to perform the parton shower, while the fast detector simulation is carried out with DELPHES [44]. In order to account for higher order corrections and additional detector effects we simulate SM $W^+W^-$ and $W^\pm Z$ productions in the fiducial region requiring the same cuts and isolation criteria adopted by the corresponding ATLAS studies, and normalize our results bin by bin to the experimental collaboration predictions for the kinematical distributions under consideration. Then we apply these correction factors to our simulated $WV$ distributions in the presence of the anomalous couplings.

The statistical confrontation of these predictions with the LHC Run 2 data is made by means of a binned log-likelihood function based on the contents of the different bins in the kinematical distribution of each channel. Besides the statistical errors we incorporate the systematic and theoretical uncertainties added in quadrature to the uncorrelated statistical error in each bin assuming some partial correlation among them which we estimate to range between 30% and 70% with the information provided. With this, we build the corresponding $\chi^2_{\text{EWDBD}}$ which we combine with the EWPD bounds so we have

$$\chi_{\text{EWPD+EWDBD}}^2(f_B, f_W, f_{WW}, f_{BW}, f_{\Phi,1}, f_{\Phi,2}, f_{\Phi,Q}, f^{(1)}_{\Phi,u}, f^{(1)}_{\Phi,d}, f^{(1)}_{\Phi,ud}, f^{(1)}_{\Phi,e}, f_{LLLL})$$

(3.3)

\footnote{Since the data points give the number of $WZ$ signal events after background subtraction their statistical error read from the figure are much larger than $\sqrt{N_i^{WW}}$.}
As for Higgs processes, we use the available data from Runs 1 and 2 from the following sources:

| Source                        | Int.Luminosity (fb$^{-1}$) | # Data points |
|-------------------------------|-----------------------------|--------------|
| ATLAS+CMS at 7 & 8 TeV [45]   | 5 & 20                      | 20+1         |
| ATLAS at 13 TeV [46]          | 79.8                        | 9            |
| CMS at 13 TeV [47]            | 35.9                        | 24           |
| ATLAS at 8 TeV [48] (γZ)      | 20                          | 1            |
| ATLAS at 13 TeV [49] (γZ)     | 36.1                        | 1            |
| ATLAS at 13 TeV [50] (µ$^+$$^-$) | 36.1                      | 1            |

that provide us signal strengths or ratios of cross sections and branching ratios. The first three references above contain information on all production mechanisms and almost all decay channels in the Figures and Tables given in the first column. Moreover, these references also provide the correlation matrix among the observables, as well as statistic and systematic errors (for Ref. [47] the correlation matrix can be found in [51]). The fourth and fifth references contains information on the rare decay mode γZ while the last one on the µ$^+$$^-$ channel.

The statistical comparison of our effective theory predictions with the LHC Runs 1 and 2 data is made by means of a $\chi^2_{Higgs}$ function based on these 22 (Run 1) + 35 (Run 2) data points. Adding this to the analysis of EWPD and EWDBD we construct our global 20 dimensional statistical function

$$\chi^2_{EWPD+EWDBD+Higgs}(\gamma_B, f_W, f_{WWW}, f_{BB}, f_{BW}, f_{GG}, f_{\Phi,1}, f_{\Phi,2}, f_{(3)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(3)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{(1)}, f_{LLL}, f_B, f_t, f_\tau, f_\mu).$$

### IV. RESULTS

We present in Figs. 1–4 $\Delta\chi^2$ profiles (in all cases marginalized with respect to all undisplayed parameters involved in the analysis) for the Wilson coefficients for three sets of analyses which differ in the data samples included:

- **EWPD:** $\Delta\chi^2_{EWPD}$ which constrains the 8 coefficients in $\Delta L_{eff}^{EWPD}$, Eq. (2.6). They are given by the green lines in Figs. 1 and 3. This analysis is performed taking into account only the contributions to the observables that are linear in the anomalous Wilson coefficients; for further detail see Ref. [26].

- **EWPD+EWDBD:** $\Delta\chi^2_{EWPD+EWDBD}$ which limits the 12 coefficients in $\Delta L_{eff}^{EWPD} + \Delta L_{eff}^{TGC}$, Eqs. (2.6) and (2.10). The results are depicted in Fig. 2. In the evaluation of the predictions for EWDBD we have kept the contribution of the Wilson coefficients up to the quadratic order.

- **GLOBAL ≡ EWPD+EWDBD+HIGGS:** $\Delta\chi^2_{EWPD+EWDBD+Higgs}$ which constrains the 20 coefficients in $L_{eff}$ in Eq. (2.15) (Eqs. (2.6)–Eqs.(2.14)). They are the red, black, and dashed blue curves in Figs. 1, 3 and 4. In the evaluation of the predictions for EWDBD and the Higgs data we have kept the contribution of the Wilson coefficients to the physical observables up to the quadratic order.

#### A. Gauge boson couplings to fermions

Our results concerning the determination of the Wilson coefficients for the operators involving gauge boson and fermion fields and which directly modify the gauge couplings to fermions are shown in Fig. 1. As it is well known, EWPD yields strong bounds on deviations of the SM predictions for the fermion-gauge interactions, and this is quantified in the green curves in the figure. The additional information provided by the inclusion of the LHC data from EWDBD and Higgs observables (now in the larger 20 parameter space) collected at Run 1 (and Run 2) are shown as the black (red) curves.

In the upper left panel of Fig. 1, we find the $\Delta\chi^2$ dependence on $f_{\Phi,1}/\Lambda^2$ which is the coefficient of the only operator involving gauge couplings to leptons remaining in the basis after applying the EOM. This operator modifies the $Z$
coupling to right-handed leptons which were precisely tested at LEP. On the contrary, at the LHC observables it enters only via its contribution to the decay rate of the $Z$ boson to leptons in some of the final states considered. Consequently, as seen in the figure, the inclusion of the LHC data does not add any meaningful information about this coefficient.

The central and right upper panels in Fig. 1 display the $\Delta \chi^2$ dependence on the coefficients $f^{(1)}_{\Phi,Q}/\Lambda^2$ and $f^{(3)}_{\Phi,Q}/\Lambda^2$, which correspond to operators modifying the couplings of left-handed quarks to $Z$ and $W$ bosons. On the other hand, the left and central lower panels correspond to the dependence on $f^{(1)}_{\Phi,u}/\Lambda^2$ and $f^{(1)}_{\Phi,d}/\Lambda^2$ which give corrections to the $u_R$ and $d_R$ couplings to $Z$ respectively. Comparing the green with the black and red lines we see that the impact of the inclusion of the LHC results is still minor but not negligible, in particular for $f^{(1)}_{\Phi,d}/\Lambda^2$. The EWPD analysis favors non-vanishing value for $f^{(1)}_{\Phi,d}/\Lambda^2$ at 2$\sigma$, a result driven by the 2.7$\sigma$ discrepancy between the observed $A^{b}_{FB}$ and the SM. On the contrary, no significant discrepancy is observed between the relevant LHC observables, in particular in EWDBD, and the SM predictions. Hence there is a shift towards zero of $f^{(1)}_{\Phi,d}/\Lambda^2$ when including the LHC data in the analysis. This slightly smaller tension results also into the reduction of the globally allowed range. This behavior was observed in Ref. [14] for Run 1 data and the inclusion of Run 2 results adds in this direction.

Finally, in the right lower panel we show the $\Delta \chi^2$ on the coefficient of $O^{(1)}_{\Phi, ud}$ operator. This operator induces a right-handed coupling of the $W$ boson to quarks. At the linear level it does not interfere with the SM and its effect has not been included in the EWPD analysis. The dependence shown in the figure arises from its contribution to the LHC observables which we keep up to the quadratic order (notice that $\Delta \chi^2$ as a function of this coupling is symmetric around zero even though its minimum is not exactly at zero). The figure illustrates how including the effect of this operator to that order leads to bounds on its coefficient which are comparable to those of the other operators that modify the coupling of electroweak gauge bosons to quarks and interfere with the SM.

FIG. 1: $\Delta \chi^2$ as a function of the fermionic Wilson coefficients $f^{(1)}_{\Phi,e}/\Lambda^2$, $f^{(1)}_{\Phi,Q}/\Lambda^2$, $f^{(3)}_{\Phi,Q}/\Lambda^2$, $f^{(1)}_{\Phi,u}/\Lambda^2$, $f^{(1)}_{\Phi,d}/\Lambda^2$, and $f^{(1)}_{\Phi, ud}/\Lambda^2$, as indicated in the panels after marginalizing over the remaining fit parameters. The green solid line stands for the fit of the EWPD that constrains only eight of twenty Wilson coefficients in Eq. (2.15). The black (red) solid line represents the twenty-parameter fit to the LHC Run 1 (and 2) data.
B. Triple anomalous gauge couplings in Diboson searches at Run 2

As mentioned in the previous section, for Run 2 the number of experimental studies focused on deriving constraints in the size and structure of TGC’s is very limited and makes use only of a small fraction of their collected data [37]. But the ATLAS collaboration has presented results on diboson production in Ref. [38, 39] which we make use to test the TGC’s; see previous section for details on our construction of the corresponding likelihood functions.

The results of our analysis of the ATLAS Run 2 WW and WZ leptonic data [38, 39] together with the EWPD in the twelve-dimensional parameter space

\[
\left\{ f_B, f_W, f_{WWW}, f_{BW}, f_{\Phi,1}, f_{\Phi,Q}, f_{\Phi,u}, f_{\Phi,d}, f_{\Phi,ud}, f_{\Phi,e} \right\}
\]

are shown in the upper panels in Fig. 2, where we plot the one-dimensional $\Delta \chi^2$ distributions for the Wilson coefficients of the “TGC operators” $\mathcal{O}_B$, $\mathcal{O}_W$ and $\mathcal{O}_{WWW}$ after marginalization over the 11 undisplayed coefficients. As expected, the WZ channel gives no constraint on $\mathcal{O}_B$ while both WW and WZ contribute with similar precision to the determination of $f_W/\Lambda^2$ and $f_{WWW}/\Lambda^2$. To illustrate the possible effect of our assumptions on the correlations of the systematic/theoretical uncertainties (labeled as SYS in the figure) among the different bins we show the results obtained with full (zero) correlation among those uncertainties in the dashed (solid) lines. As seen in the figure the effect is small.

In the lower panels we show the impact of adding the Run 2 WW and WZ results to the analysis of the Run 1 diboson data of Ref. [14] which included data on WW and WZ channels from both ATLAS and CMS collected with $\sim 20 \text{ fb}^{-1}$ at each experiment. Altogether we find that the combined ATLAS Run 2 diboson data constrains the operator coefficients with precision similar (a bit better indeed) to that of the full Run 1 analysis. This is expected from simple statistics of the integrated luminosity and energy scaling. The combination of CMS and ATLAS Run 1 data accounts for about 40 fb$^{-1}$ in each WW and WZ channels which is of the order of the 36 fb$^{-1}$ of ATLAS Run 2 data. Moreover, the total cross section for diboson productions is about twice larger at Run 2 than at Run 1.

C. Higgs couplings

Our results concerning the determination of the Wilson coefficients for the operators affecting the interactions of the Higgs field with the gauge bosons and with fermions are shown in Figs. 3 and 4 respectively. In order to perform the most general analysis of the Higgs boson couplings we use the full data set that we presented in Section [11] i.e. EWPD, EWDBD and Higgs data, including the effect of the 20 operators in Eq. (2.15).

Figure 3 depicts the one-dimensional $\Delta \chi^2$ as a function of the Wilson coefficients of the pure bosonic operators in Eq. (2.15) after fitting the EWPD and Run 1 (and 2) data on Higgs and diboson productions. As expected, the most stringent constraints are those on the oblique operators $\mathcal{O}_{\Phi,1}$ and $\mathcal{O}_{BW}$ that come from the EWPD with very little impact of the LHC data [11].

The first row of Fig. 3 contains the $\Delta \chi^2$ distributions for the coefficients of the “TGC operators”. Of those only $\mathcal{O}_B$ and $\mathcal{O}_W$ enter both in TGC’s and Higgs processes. For completeness we include here the results of our global analysis on $f_{WWW}/\Lambda^2$ also but we notice that $\mathcal{O}_{WWW}$ does not involve the Higgs field. As we can see, altogether the inclusion of the Run 2 data improves the bounds on the coefficients of the three “TGC operators” by a factor $\mathcal{O}(25\%)$. Also comparing the results for these operators to the second row of Fig. 3 we learn that the inclusion of the Higgs data set strengthens the bounds on $f_B/\Lambda^2$ and $f_W/\Lambda^2$ derived from the EWDBD analysis by $\mathcal{O}(10 - 20\%)$ [52].

The operators $\mathcal{O}_{BB}$ and $\mathcal{O}_{WW}$ modify the Higgs decay into two photons with a contribution proportional to $f_{BB}/\Lambda^2 + f_{WWW}/\Lambda^2$, therefore, introducing a strong correlation between these operators [6] since the decay rate for this Higgs channel is very well measured. This is illustrated in Fig. 5 where we show the two-dimensional allowed regions from the global analysis for different pairs of Wilson coefficients after marginalizing over the 18 undisplayed parameters in each panel. In particular on the left panel we show the degree of anti-correlation between $f_{BB}/\Lambda^2$ and
FIG. 2: $\Delta\chi^2$ dependence on the $f_B/\Lambda^2$ (left panel), $f_W/\Lambda^2$ (central panel) and $f_{WWW}/\Lambda^2$ (right panel) parameters after the marginalization over the 11 undisplayed fit parameters for the analysis of LHC EWDBD and EWPD. The upper panels show the results of our analysis of the ATLAS Run 2 data on $WZ$ [38] and on $WW$ [39] transverse mass distributions. Full lines (dashed) correspond to assuming zero (total) correlation among the non-statistical uncertainties; see text for details. The lower panels show the results of the analysis of the EWDBD from Run 1 of Ref. [14] in combination with EWPD (black lines) and including also the results from ATLAS $WW$ and $WZ$ production at Run 2 (red line).

$f_{WW}/\Lambda^2$ still present after combination of Run 1 and 2 data. We also see the two quasi-degenerate solutions discussed in Eq. (2.19), the lower one containing the SM solution ($f_{WW} = f_{BB} = 0$) and the upper one with flipped sign of the $H\gamma\gamma$ coupling “displaced” by $\sim 3$ TeV$^{-2}$.

The lower row of Fig. 3 contains the results for $f_{GG}/\Lambda^2$ and $f_{\Phi,2}/\Lambda^2$ which clearly display the discrete (quasi-) degeneracies explained in Section II (see discussions around Eqs. (2.18) and (2.16)) associated with the reversion of the sign of the $Hgg$ and $HVV$ ($V = Z, W$) couplings respectively. Notice that the two solutions for $f_{GG}/\Lambda^2$ are completely equivalent in the analysis since this coupling only appears in one vertex. On the other hand, the operator $O_{\Phi,2}$ modifies universally all the SM-like Higgs couplings to gauge bosons and fermions. For each of them there are two degenerate solutions due to the total reversal of the coupling sign, but they would only lie at exactly the same values of $f_{\Phi,2}/\Lambda^2$ if all the couplings were measured to have the same ratio to their SM value. The quasi-degeneracy in $f_{\Phi,2}/\Lambda^2$ present in our global analysis originates from the lack of tension between the SM predictions and the data for all processes so values around $f_{\Phi,2}/\Lambda^2 \sim 0$ and $f_{\Phi,2}/\Lambda^2 \sim \frac{1}{3}$ with all other couplings zero can lead to a good global description of the data. As seen in the figure, the addition of Run 2 data has contributed in this direction.

We display in Fig. 4 the $\Delta\chi^2$ dependence on the Wilson coefficients of the operators generating anomalous Yukawa couplings. Comparing the results obtained using just the LHC Run 1 data set (black curve) with the ones that contains the LHC Run 2 data (red curve), we can see that the Run 2 data is essential to better constrain these Wilson coefficients. For instance, we can witness the emergence of the three discrete solutions for $f_b/\Lambda^2$ and $f_\tau/\Lambda^2$ which originate from Eqs. (2.16) and (2.17) as explained in Section II. On the other hand, it is clear from this figure that the data on Higgs decay into muon pairs is still incipient and within the present precision the allowed regions around the three minima merge into a unique allowed range.
FIG. 3: $\Delta \chi^2$ dependence on the bosonic Wilson coefficients $f_B/\Lambda^2$, $f_W/\Lambda^2$, $f_{WW}/\Lambda^2$, $f_{BB}/\Lambda^2$, $f_{WWW}/\Lambda^2$, $f_{BB}/\Lambda^2$, $f_{WW}/\Lambda^2$, $f_{BW}/\Lambda^2$, $f_{GG}/\Lambda^2$, $f_{\Phi}/\Lambda^2$, and $f_{\Phi}/\Lambda^2$ as indicated in each panel. The black (red) line stands for the results of the twenty-parameter fit using EWPD, EWDBD and Higgs data from LHC Run 1 (and 2). As before, the green line stands for the fit of only the EWPD.

We show in this figure the results of the global analysis under two assumptions for the top-Higgs associate production in Run 2. As described in Ref. [46] both $ttH$ and $tH$ (including $tHW$ and $tHj$) contribute to the cross section ratio given in Fig. 6 of that reference. But with the information provided, it is not possible to determine the relative contribution of $tH$ vs $ttH$ to the reconstructed total cross section ratio. We show the results for two extreme assumptions: a ratio of the $tH$ to $ttH$ contribution as predicted by the model (i.e. exactly same reconstruction efficiency for both subprocesses), shown as the dashed blue lines in the figure, and a negligible small contribution from $tH$ shown in the red line. For consistency, we see that the results for all non-top Yukawa couplings are exactly the same for the two analyses. For $f_{t}/\Lambda^2$ we find that including a “full” $tH$ contribution results into the total breaking of the degeneracies and eliminates solutions other than the ones around $f_{t}/\Lambda^2 = 0$. This can also be seen in the right panel in Fig. 3 where we show the allowed regions in the plane $f_{t}/\Lambda^2$ vs $f_{\Phi}/\Lambda^2$. The void and colored regions of this panel show the four solutions resulting from Eqs. (2.16) and (2.17) explained in Section II which are quasi-degenerated as long as no information on the sign of the $ttH$ coupling is available. On the other hand, the colored regions are the only ones allowed once the information on $tH$ is included in the analysis as described above. This is expected as the $tH$ scattering amplitude receives contributions from the $ttH$ and VVH vertices, therefore, being sensitive to the relative sign of the different diagrams contributing to it. In fact, the sign with respect to the SM of the vertices $ttH$
and $VVH$ are the same in the surviving colored regions in Fig. [5] This result clearly illustrates the importance of the measurement of the $tH$ production rate to unambiguously determine the coupling of the Higgs to the top quark.

**FIG. 4:** $\Delta \chi^2$ dependence on the fermionic Wilson coefficients $f_b/\Lambda^2$, $f_t/\Lambda^2$, $f_\tau/\Lambda^2$, and $f_\mu/\Lambda^2$ as indicated in each panel. The black (blue) line stands for the results of the twenty-parameter fit using EWPD, diboson production and Higgs data from LHC Run 1 (and 2). The red line represents that results obtained using EWPD, diboson production and Higgs data from LHC Run 1 and 2 without the $tH$ contribution to the Higgs top associate production cross section (see text for details).

**FIG. 5:** $1\sigma$ and 95% CL (2dof) allowed regions from the global analysis in the planes indicated in the axes. In the right panel the filled regions are obtained from the global analysis including the $tH$ contribution to the top Higgs associate production data of ATLAS at Run 2 while the void regions are the additional solutions allowed when the $tH$ contribution is not included.
D. Results at linear order

In order to interpret Eq. (2.1) as a systematic expansion in the large mass parameter $\Lambda$, its contributions to observables at the lowest order ($1/\Lambda$) are given the interference between anomalous and SM terms. In principle, if one keeps the quadratic contributions on the Wilson coefficients of dimension–six operators one should include the interference of dimension–eight operators with the SM as they are of the same order.

Up to this point we consider the effective lagrangian Eq. (2.15) as a straw man that we use to probe the standard model couplings assuming that it contains all information on possible new physics. The results obtained are thus physically meaningful as long as no large cancellations between the dimension–six quadratic terms and the (here absent) linear dimension–eight SM interference are expected. Furthermore, this is a pragmatic approach since there are phase space regions where the lowest order systematic expansion fails [13] that is signaled by the cross section being negative! Notwithstanding, the use of the quadratic contributions of the dimension–six operators is justified if the new physics is strongly interacting; see for instance Refs. [53–55]. Indeed, this result is consequence of Naive Dimensional Analysis [56] and some simple power counting analysis. In any case, Ref. [57] shows that the analysis of the LHC data in terms of dimension–six operators is adequate in almost all realistic weakly coupled scenarios, except in the high energy tails of distributions.

At this point we would like to understand the importance of keeping the anomalous quadratic terms in the evaluation of the observables. The result of this exercise certainly depends on the amount of data available. To this end, we redid our twenty-parameter fit using only the contributions to the observables at linear order on the Wilson coefficients; our results are depicted in Fig. 6. Comparing the results of the dashed curves in Fig. 6 with the green curves in Fig. 1 we can see that the $\Delta \chi^2$ distributions as a function of $(f_{BW}, f_{\Phi,1}, f_{\Phi,2}, f_{\Phi,3}, f_{\Phi,4}, f_{\Phi,5}, f_{\Phi,6}, f_{\Phi,7}, f_{\Phi,8}, f_{LLLL})$ are very much the same as obtained using only the EWPD (see also Table III). This shows that the contributions to these parameters due to diboson and Higgs data arise mainly from the quadratic terms. Moreover, within the input range of variation of the parameters in the analysis, the operator $O_{\Phi,ud}$ is not bounded if the observables are evaluated using just the linear terms of their Wilson coefficients while and $O_{WWW}$ is only very weakly constrained. This happens because the dominant contributions of these operators are to helicity amplitudes to which the SM does not contribute [14].

The results in Fig. 6 show that the Higgs data is already precise enough to determine $f_{\Phi,2}/\Lambda^2$ and $f_{GG}/\Lambda^2$ in the linear approximation with the quadratic terms being subdominant. Moreover, as expected, at linear order there are no degenerate solutions in these couplings and the allowed regions encompass only the SM. Same applies to the Yukawa-like operators so the corresponding coefficients $f_f/\Lambda^2$ have no degenerate solutions. And therefore the $f_\mu/\Lambda^2$ seems better determined.

We also find that at present the Higgs data is precise enough to bound the couplings $f_{BB}/\Lambda^2$ and $f_{WW}/\Lambda^2$ using the linear approximation of the observables, however, the size of the 95% CL allowed area increases by a factor of $\sim 2$. Similarly the bounds on $f_{B}/\Lambda^2$ and $f_{W}/\Lambda^2$ are a factor of $\mathcal{O}(3 - 4)$ weaker than those obtained when we include the quadratic terms [52]. Nevertheless, this is already very interesting since the diboson production alone does only lead to very mild bounds on these last two couplings when not including the quadratic contributions, which indicates again the relevance of the Higgs observables.

V. SUMMARY

In this work we have performed a comprehensive analysis of the observables related to the electroweak sector, which at present allows for precision tests of the couplings between electroweak gauge bosons and fermions, triple electroweak gauge couplings and the couplings of the Higgs to fermions and gauge bosons. This includes low energy electroweak precision measurements as well as LHC data on gauge boson pair production and Higgs observables. In total, the GLOBAL analysis of EWPD and EWDBD and Higgs results from LHC Run 1 encompasses 64 observables and including Run 1 and 2, 122 observables.
FIG. 6: $\Delta \chi^2$ dependence on the bosonic Wilson coefficients $f/\Lambda^2$ as indicated in each panel. The results using only the linear terms in the anomalous couplings are indicated by the blue dotted curves. The red solid curves stands for the fits keeping the quadratic contributions of the anomalous couplings to the observables. The full data set was used in both cases.

We work in the framework of effective lagrangians with a linear realization of the electroweak symmetry. At dimension six, and assuming that the new operators do not introduce new tree level sources of flavor violation nor violation of universality of the weak current, the global analysis involves the 20 operators in Eq. (2.15) of which 8 contribute to EWPD (Eq. (2.6)), 4 additional enter in the combination with the LHC EWDBD (Eq. (2.10)), and the 20 operators enter once the Higgs observables are considered.

Altogether the analyses show no statistically significant source of tension with the SM. We find for the SM a $\chi^2_{\text{SM}} = 118 (71.2)$ for the 122 (64) observables in the GLOBAL analysis of EWPD and EWDBD and Higgs results from LHC Run 1+2 (only Run 1). Including the 20 Wilson coefficients in the fit, we find $\chi^2_{L_{eff}} = 91 (52.3)$. As a consequence, bounds on the Wilson coefficients can be imposed. The 95% allowed ranges for the 20 Wilson coefficients (profiled from the global 9-,12-, or 20-dimensional likelihoods) are listed in Table III

The corresponding allowed 95%
| Operator  | EWPD | EWPD+EWDBD | GLOBAL Run 1 | GLOBAL Run 1+2 | GLOBAL Run1+2 Linear |
|-----------|------|------------|--------------|----------------|---------------------|
| $O_{LLLL}$ | (-0.043, 0.013) | (-0.043, 0.013) | (-0.043, 0.013) | (-0.043, 0.013) | (-0.043, 0.013) |
| $O_{\Phi,1}$ | (-0.075,0.011) | (-0.075,0.007) | (-0.077,0.009) | (-0.075,0.007) | (-0.077,0.005) |
| $O_{BW}$ | (-0.040,0.15) | (-0.040,0.15) | (-0.043,0.15) | (-0.044,0.14) | (-0.034,0.15) |
| $O_{\Phi,Q}$ | (-0.32,1.7) | (-0.27,1.7) | (-0.32,1.7) | (-0.30,1.7) | (-0.21,1.8) |
| $O_{\Phi,1}$ | (-0.083,0.10) | (-0.034,0.11) | (-0.049,0.11) | (-0.036,0.11) | (-0.089,0.088) |
| $O_{\Phi,1}^{(1)}$ | (-1.2,-0.13) | (-0.64,-0.007) | (-0.73,0.02) | (-0.56,0.04) | (-1.0,-0.03) |
| $O_{\Phi,u}^{(1)}$ | (-0.25,0.37) | (-0.17,0.37) | (-0.22,0.38) | (-0.19,0.33) | (-0.32,0.25) |
| $O_{\Phi,1}$ | (-7.8,3.5) | (-5.2,3.5) | (-3.0,3.7) | (-9.5,13) |
| $O_{\Phi,u}^{(1)}$ | (-25,20) | (-12,17) | (-8,12) | (-14,21) |
| $O_{\Phi,1}$ | (-62,20) | (-3.2,20) | (-6.2,20) | (-6.2,20) |
| $O_{\Phi,1}$ | (-64,35) | (-19,20) | (-7.4,20) | (-7.4,20) |
| $O_{\Phi,1}$ | (-59,31) | (-5.8,31) | (-5.8,31) | (-5.8,31) |

TABLE III: 95% allowed ranges for the Wilson coefficients for the different analysis performed in this work. For $O_{\Phi,1}$ we show in the 5th column the three discrete ranges allowed when no contribution of $tH$ is included in the ATLAS cross section ratio. Including the $tH$ contribution under the assumptions discuss in the text selects the range around zero which we mark with square brackets.

CL ranges for the global analysis with Run 1 and Run 1 + 2 EWDBD and Higgs observables are also graphically displayed in Fig. [7]

In brief, we find:

- The coefficients of the eight operators contributing to the EWPD are those better determined, as could be anticipated. The inclusion of the LHC EWDBD and Higgs observables has negligible impact on those operators contributing to the couplings of leptons, $O_{LLLL}$, $O_{\Phi,e}^{(3)}$, $O_{\Phi,1}$, and $O_{BW}$.

- The impact of the inclusion of the LHC results is still minor but not negligible for the EWPD bounded operators involving gauge couplings to quarks. In particular for $f_{\Phi,d}^{(1)}/A^2$, under the assumption of generation universality a non-zero value for this coefficient is favored in the EWPD analysis coming from the 2.7$\sigma$ discrepancy between the observed $A_{FB}^{0,b}$ and the SM. On the contrary, LHC observables involving this operator, are fully consistent with the SM what results in the shift and reduction of its globally allowed range.

- The operator $O_{\Phi,1}^{(1)}$ induces right-handed charged current couplings for quarks and it can only be bound via its quadratic contributions. Including those in the LHC observables its Wilson coefficient can be bounded with precision comparable to that of the other operators affecting gauge-quark couplings.

- We have performed a novel analysis of the Run 2 ATLAS 36.1 fb$^{-1}$ data on transverse mass distribution of $W^+W^−$ and $W^±Z$ in the leptonic channel [38, 39] which allows for further tests of the TGC’s. The results are shown in Fig. [2]. We find that the combined ATLAS Run 2 diboson data constrains the operator coefficients with precision similar (a bit better indeed) to that of the full Run 1 analysis.
Inclusion of the Run 2 results in the global analysis results into a reduction of the allowed range for the coefficients of the bosonic operators $O_B$, $O_W$, $O_{WWW}$, $O_{BB}$, and $O_{WW}$ by 20–30%.

The allowed values for $f_{GG}/\Lambda^2$ and $f_{\Phi,2}/\Lambda^2$ present each two discrete ranges originated by the degeneracy (it is a quasi-degeneracy for $f_{\Phi,2}$) associated with the reverse of the sign of the $Hgg$ (Eq. (2.18)) and $HXX$ ($X = f, V$) (Eqs. (2.16), (2.17)), respectively. Barring that degenerate solutions these are the best determined coefficients for operators not contributing to EWPD.

The allowed values for the coefficients for the Yukawa-like operators $O_{d\Phi,33}$ and $O_{e\Phi,33}$ ($f_t$, and $f_\tau$), have a twofold degeneracy associated with the reverse of the sign of the corresponding $Hff$ coupling (see Eq. (2.17)) in combination with the reverse of the sign of the $HVV$ coupling. This results into the three discrete allowed ranges in Table III. For the $O_{e\Phi,22}$ coefficient, $f_\mu$, the data is not precise enough to resolve the three solutions.

For $O_{u\Phi,33}$, the inclusion of the incipient $tH$ data can break those degeneracies on $f_t$, this is, in the determination of the top-Higgs coupling.

The last column in Table III shows the allowed ranges when only the terms linear in the Wilson coefficients are kept in the observables. For those operators constrained by EWPD the bounds are just that of the EWPD as at LHC they are mainly constrained by its quadratic contribution. For the operators without degenerate solutions the bounds become weaker but are still within the same order or magnitude. Exceptions are $O_{q,ud}^{(1)}$ and $O_{WW}$ which become very weakly bounded as their dominant contributions at LHC are to helicity amplitudes which do not interfere with the SM ones. Keeping only the linear contribution to the observables does not allow for the degenerated solutions associated with the sign flip of the Higgs couplings. Consequently $f_{GG}/\Lambda^2$, $f_{\Phi,2}/\Lambda^2$, $f_B/\Lambda^2$, $f_t/\Lambda^2$, $f_\tau/\Lambda^2$, and $f_\mu/\Lambda^2$ appear to be better constrained.

Our results show the importance of the Higgs data to constrain the TGC operators $O_B$ and $O_W$ when the LHC observables are evaluated using only the linear terms in the anomalous couplings. This extends the previous results in Refs. [52, 58].
Altogether we find that the increased integrated luminosity gathered at 13 TeV allows us to obtain more stringent bounds on a larger set of anomalous interactions and to perform new tests of the SM. We look forward for the release of the complete dataset accumulated at Run 2.

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[1] G. Aad et al. (ATLAS), Phys. Lett. B716, 1 (2012), 1207.7214.
[2] S. Chatrchyan et al. (CMS), Phys. Lett. B716, 30 (2012), 1207.7235.
[3] S. Weinberg, Physica A96, 327 (1979).
[4] H. Georgi, Weak Interactions and Modern Particle Theory (1984), ISBN 9780805331639.
[5] J. F. Donoghue, E. Golowich, and B. R. Holstein, Camb. Monogr. Part. Phys. Nucl. Phys. Cosmol. 2, 1 (1992), [Camb. Monogr. Part. Phys. Nucl. Phys. Cosmol.35(2014)].
[6] T. Corbett, O. J. P. Éboli, J. González-Fraile, and M. C. González-García, Phys. Rev. D86, 075013 (2012), 1207.1344.
[7] T. Corbett, O. J. P. Éboli, J. González-Fraile, and M. C. González-García, Phys. Rev. D87, 015022 (2013), 1211.4580.
[8] T. Corbett, O. J. P. Éboli, D. Goncalves, J. González-Fraile, T. Plehn, and M. Rauch, JHEP 08, 156 (2015), 1505.05516.
[9] A. Butter, O. J. P. Éboli, J. Gonzalez-Fraile, M. C. Gonzalez-Garcia, T. Plehn, and M. Rauch, JHEP 07, 152 (2016), 1604.03105.
[10] J. Ellis, C. W. Murphy, V. Sanz, and T. You, JHEP 06, 146 (2018), 1803.03252.
[11] C. Grojean, M. Montull, and M. Riembau (2018), 1810.05149.
[12] Z. Zhang, Phys. Rev. Lett. 118, 011803 (2017), 1610.01618.
[13] J. Baglio, S. Dawson, and I. M. Lewis, Phys. Rev. D96, 073003 (2017), 1708.03332.
[14] A. Alves, N. Rosa-Agostinho, O. J. P. boli, and M. C. Gonzalez-Garcia, Phys. Rev. D98, 013006 (2018), 1805.11108.
[15] S. Weinberg, Phys. Rev. Lett. 43, 1566 (1979).
[16] B. Grzadkowski, M. Iskrzynski, M. Misiak, and J. Rosiek, JHEP 10, 085 (2010), 1008.4884.
[17] H. D. Politzer, Nucl. Phys. B172, 349 (1980).
[18] H. Georgi, Nucl. Phys. B361, 339 (1991).
[19] C. Arzt, Phys. Lett. B342, 189 (1995), hep-ph/9304230.
[20] H. Simma, Z. Phys. C61, 67 (1994), hep-ph/9307274.
[21] K. Hagiwara, S. Ishihara, R. Szalapski, and D. Zeppenfeld, Phys. Rev. D48, 2182 (1993).
[22] K. Hagiwara, T. Hatsukano, S. Ishihara, and R. Szalapski, Nucl. Phys. B496, 66 (1997), hep-ph/9612268.
[23] S. Schael et al. (SLD Electroweak Group, DELPHI, ALEPH, SLD, SLD Heavy Flavour Group, OPAL, LEP Electroweak Working Group, L3), Phys. Rept. 427, 257 (2006), hep-ex/0509008.
[24] A. De Rujula, M. B. Gavela, P. Hernandez, and E. Masso, Nucl. Phys. B384, 3 (1992).
[25] J. Elias-Miro, J. R. Espinosa, E. Masso, and A. Pomarol, JHEP 11, 066 (2013), 1308.1879.
[26] T. Corbett, O. J. P. Éboli, and M. C. Gonzalez-Garcia, Phys. Rev. D96, 035006 (2017), 1705.09294.
[27] T. Corbett, O. J. P. Éboli, and M. C. Gonzalez-Garcia, Phys. Rev. D91, 035014 (2015), 1411.5026.
[28] C. Patrignani et al. (Particle Data Group), Chin. Phys. C40, 100001 (2016).
[29] L. E. W. Group (Tevatron Electroweak Working Group, CDF, DELPHI, SLD Electroweak and Heavy Flavour Groups, ALEPH, LEP Electroweak Working Group, SLD, OPAL, D0, L3) (2010), 1012.2367.
[30] M. Ciuchini, E. Franco, S. Mishima, M. Pierini, L. Reina, and L. Silvestrini, in *International Conference on High Energy Physics 2014 (ICHEP 2014) Valencia, Spain, July 2-9, 2014* (2014), 1410.6940.

[31] The LEP Collaborations ALEPH, DELPHI, L3, OPAL, and the LEP TGC Working Group, *A Combination of Preliminary Results on Gauge Boson Couplings Measured by the LEP Experiments*, http://lepewwg.web.cern.ch/LEPEWWG/lepww/tgc

[32] G. Aad et al. (ATLAS), JHEP **09**, 029 (2016), 1603.01702.

[33] V. Khachatryan et al. (CMS), Eur. Phys. J. **C76**, 401 (2016), 1507.03268.

[34] G. Aad et al. (ATLAS), Phys. Rev. **D93**, 092004 (2016), 1603.02151.

[35] V. Khachatryan et al. (CMS), Eur. Phys. J. **C77**, 236 (2017), 1609.05721.

[36] K. Hagiwara, R. D. Peccei, D. Zeppenfeld, and K. Hikasa, Nucl. Phys. **B282**, 253 (1987).

[37] ATLAS Collaboration, ATLAS-CONF-2016-043, https://cds.cern.ch/record/2206093

[38] ATLAS Collaboration, ATLAS-CONF-2018-034, https://cds.cern.ch/record/2630187

[39] M. Aaboud et al. (ATLAS), Eur. Phys. J. **C78**, 24 (2018), 1710.01123.

[40] J. Alwall, R. Frederix, S. Frixione, V. Hirschi, F. Maltoni, O. Mattelaer, H. S. Shao, T. Stelzer, P. Torrielli, and M. Zaro, JHEP **07**, 079 (2014), 1405.0301.

[41] N. D. Christensen and C. Duhr, Comput. Phys. Commun. **180**, 1614 (2009), 0806.4194.

[42] A. Alloul, N. D. Christensen, C.Degrande, C. Duhr, and B. Fuks, Comput. Phys. Commun. **185**, 2250 (2014), 1310.1921.

[43] T. Sjostrand, S. Mrenna, and P. Z. Skands, JHEP **05**, 026 (2006), hep-ph/0603175.

[44] J. de Favereau, C. Delaere, P. Demin, A. Giammanco, V. Lemaitre, A. Mertens, and M. Selvaggi (DELPHES 3), JHEP **02**, 057 (2014), 1307.6346.

[45] G. Aad et al. (ATLAS, CMS), JHEP **08**, 045 (2016), 1606.02266.

[46] ATLAS Collaboration, ATLAS-CONF-2018-031, https://cds.cern.ch/record/2629412

[47] A. M. Sirunyan et al. (CMS), Submitted to: Eur. Phys. J. (2018), 1809.10733.

[48] G. Aad et al. (ATLAS), Eur. Phys. J. **C76**, 6 (2016), 1507.04548.

[49] M. Aaboud et al. (ATLAS), JHEP **10**, 112 (2017), 1708.00212.

[50] ATLAS Collaboration, ATLAS-CONF-2018-026, http://cds.cern.ch/record/2628763

[51] A. M. Sirunyan et al. (CMS), Submitted to: Eur. Phys. J. (2018), 1809.10733.

[52] T. Corbett, O. J. P. Éboli, J. González-Fraile, and M. C. González-Garcia, Phys. Rev. Lett. **111**, 011801 (2013), 1304.1151.

[53] A. Biekter, A. Knochel, M. Krmer, D. Liu, and F. Riva, Phys. Rev. **D91**, 055029 (2015), 1406.7320.

[54] R. Contino, A. Falkowski, F. Goertz, C. Grojean, and F. Riva, JHEP **07**, 144 (2016), 1604.06444.

[55] A. Falkowski, M. Gonzalez-Alonso, A. Greljo, D. Marzocca, and M. Son, JHEP **02**, 115 (2017), 1609.06312.

[56] A. Manohar and H. Georgi, Nucl. Phys. **B234**, 189 (1984).

[57] J. Brehmer, A. Freitas, D. Lopez-Val, and T. Plehn, Phys. Rev. **D93**, 075014 (2016), 1510.03443.

[58] F. de Campos, M. C. Gonzalez-Garcia, and S. F. Novaes, Phys. Rev. Lett. **79**, 5210 (1997), hep-ph/9707511.