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Integration of Expectation Maximization using Gaussian Mixture Models and Naïve Bayes for Intrusion Detection

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ABSTRACT

Intrusion detection is the investigation process of information about the system activities or its data to detect any malicious behavior or unauthorized activity. Most of the IDS implement K-means clustering technique due to its linear complexity and fast computing ability. Nonetheless, it is Naïve use of the mean data value for the cluster core that presents a major drawback. The chances of two circular clusters having different radius and centering at the same mean will occur. This condition cannot be addressed by the K-means algorithm because the mean value of the various clusters is very similar together. However, if the clusters are not spherical, it fails. To overcome this issue, a new integrated hybrid model by integrating expectation maximizing (EM) clustering using a Gaussian mixture model (GMM) and naïve Bayes classifier have been proposed. In this model, GMM give more flexibility than K-Means in terms of cluster covariance. Also, they use probabilities function and soft clustering, that’s why they can have multiple cluster for a single data. In GMM, we can define the cluster form in GMM by two parameters: the mean and the standard deviation. This means that by using these two parameters, the cluster can take any kind of elliptical shape. EM-GMM will be used to cluster data based on data activity into the corresponding category.

Keywords:
Anomaly detection
Clustering
EM classification
Expectation maximization (EM)
Gaussian mixture model (GMM)
GMM classification
Intrusion detection
Naïve Bayes classification

1. Introduction

Recently, through their networks, many organizations have encountered heavy network use. The large technological expansion that followed these networks, however, gave them different threads. Such threads include many types of malicious programs that affect network efficiency or unauthorized network access to data. This has encouraged work to strengthen and develop new ways of addressing and mitigating these threats. Any unauthorized operation on a computer network constitutes a network intrusion [1].

Intrusion detection is a “species of security technology that can collect information from some of the network or computer system’s key points and attempt to analyze it to assess whether there is a violation of the security policy or a suspicion of the computer system’s network attack.” Intrusion detection methods are classified into two groups according to the different objects for intrusion detection. One is called the identification of anomaly that is used to detect the unknown intrusion. And the other is called detection of abuse, which is used to detect the identified intrusion.

Mixed intrusion detection techniques have been fo-
2. Related Work

Dorothy Denning first described intrusion detection in 1987 [2]. According to him, “network intrusion can be detecting by monitoring network activity in terms of data and then the system can generate alerts and responses before the infringement”. Instantaneously is one of the key features of intrusion. Snort IDS applied the rule-based intrusion detection method [3, 4]. Rule-based detection system has quick detection characteristics, but it has a big problem. It cannot detect other than pre-defined types of attack. Since intruders will frequently change their technique of attack, which is often riskier. For this case, this approach cannot adopt itself such that it has not been suitable in new types of attacks. It also has a higher false alarm rate.

Intrusion detection using data mining technique requires extensive data collection in advance. Large quantities of data limit the rate of online detection [5]. Conventional intrusion detection methods are being developed using data mining [6–7] and common file analyzed [8]. In differential analyzes performed by Fisher, an et al. [9] used the approach of combining the minimum scatter class with a traditional support vector (SVM) analysis and then implemented a minimum scatter support class vector (WCS-SVM) analysis, which is better than traditional SVM. Kabir et al. [10] suggested a vector based intrusion detection method (LS-SVM) that supports the least squares, called (LS-SVM) method. The new method of improved decision mapping for intrusion detection was introduced by M. Gudadhe, Al. [11] to develop an intermediate classifier for multiple decision makers. Sufyan et al. [12] used backpropagation models for artificial neural networks to detect intrusion, encouraging intrusion detection system to adapt more effectively respond to new environments and new attack types. The vast scale of the network data set takes time and effort for manual tagging. The classification of the dataset is therefore subject to clustering methods [13]. The Ymeans clustering algorithm [14] surmounts two disadvantages of K-means clustering. This is dependency and deterioration of k-means by splitting the set of data automatically into a correct number of clusters. The k-means clustering algorithm is a simple algorithm that solves the complexity of previous clustering algorithms. Traditional SOM algorithm has some disadvantages like, not providing accurate result while clustering. This has been overcome by integration of SOM and k-means [15]. One of the major problems in clustering is to determine the cluster center and number of clusters. High speed, high detection can be achieved by the parallel clustering integration algorithm [16] for IDS. The ANN classifier [17] has a good performance in the detection of intrusion. Research in [18–20] uses a mixed learning approach to have a higher detection. Shah et al. [21] compared directly to the Snort intrusion detection system and the machine learning detection performance and found the better performance in machine learning detection system.

Sheng Yi Jang et al. proposed a clustering-based intrusion detection method [22] wherein clusters consist of unlabeled datasets and have been classified as normal or abnormal by their external factors. This method’s time complexity is linear with the dataset size and number of attributes. A method for anomaly detection by clustering regular user behavior is proposed by Sang Hyum Oh et al. [23] to model a user’s typical behavior using the clustering algorithm. Clustering prevents statistical analysis causing inaccuracy. Therefore, the user’s daily habits are more reliable than the statistical analysis.

Tasi and Lin use K-Means clustering in K-clusters to cluster data instances [24]. Next the study trains the latest dataset consisting only of cluster centers with support vector machine (SVM). They managed to achieve a high precision rate for nearly all types of attacks. This approach provides a high rate of detection but comes with a high false alarm rate.

The new approach of the IDS based on the Artificial Neural Network (ANN) with the clusters ANN and Fuzzy FC-AN Network, is suggested by Gang, Jin Xing and Jian [25]. Before a similar ANN model is trained, fuzzy clustering is carried out to formulate different models to produce different training subsets. A fuzzy module of aggregation is then used to sum the result. The subset of the training set is less complex with the use of fuzzy clusters that help the ANN learn from each subset more effectively and to detect low frequency attacks such as U2R and R2L attacks. Nevertheless, in contrast with the Naïve Bayes approach, this approach results in a lower detection rate for probing attacks.
Shaohua et al. [26] suggested detection of intrusion based on Fuzzy SVMs (FSVM) to improve classification accuracy. The clustering algorithm’s aim is to build a new training set using cluster centers. This new set will then be trained to get a support vector with FSVM. Although their findings have shown that the accuracy rate has been improved by this approach, it is not an adequate percentage.

Amiri et al. [27] used a feature selection method to improve the performance of existing classifiers by eliminating unimportant features like SVM with heavy computational challenges for large datasets. The authors have recently introduced the support vector machine of an improved least squire called PLSSVM. PLSSVM performs well in the classification of normal records and probes but misses many dynamic attacks that are very similar to normal behavior, such as DOS and U2R.

Horng [28] suggested hierarchical clustering of SVM-based IDS BIRCH as a pre-processing step and a basic feature selection method to remove unimportant features. The hierarchical clustering algorithm enhances SVM’s efficiency while the simple selection of features allows the SVM model to properly classify some data. As this method was unable to differentiate between R2L and Normal data, the percentage of predictions for this class dropped dramatically.

In terms of classification accuracy and AUC, Huang, Lu and Ling [29] performed a comparative study of Naïve Bayes, Decision tree and SVM. They found that both Naïve Bayes and SVM have very similar predictive accuracy as well as similar AUC scores are produced.

Roshan Chitrakar and Huang Chauanhe proposed a hybrid anomaly detection approach using K-medoids clustering and support vector machine classification [30]. Since there may be too many support vectors in the case of using a high dimensional kernel, this also reduces the training speed, KMeans / Medoids needs a large sample and can only handle spherical shape.

S. Varuna and Dr. P. Natesan proposed an integrated model of K- Means clustering and Naïve Bayes classification for intrusion detection [1]. The integrated algorithm improved the detection rate for the normal, Probe, R2L and U2R attacks, but it does not meet the requirements for DOS.

This paper is organized as follows: Section 3 describes the proposed work and the implementation details. Section 4 contains the results and discussion.

### 3. Proposed Model

In this research an integrated model has been proposed. This is the integration of Expectation Maximization using Gaussian Mixture Model clustering and Naïve Bayes classifier. Data are clustered and formed five clusters with outlier. The purpose of clustering is to label the data with enhancing the accuracy and performance of model by improving capacity of parallel processing of the model. Thus, clustered data with outlier are then classified using Naïve Bayes classifier.

#### 3.1 Description of Dataset

Each dataset record reflects a 41-feature network connection. Among them, 7 are nominal features, 34 are continuous features and a label. Label indicates that the data is either in normal status or in one of the 39 identified attack status. The NSL-KDD data can be categorized as either a standard class or one of four attack classes, i.e. remote to local, denial of service, Users to root and Probe classes.

Table 3.1 lists the number of instances in the training and testing data set of every type of attack group and the total number of instances in each data set.

| Attack Class          | Training data size | Test data size |
|-----------------------|--------------------|---------------|
| Normal                | 67343              | 9711          |
| Probe                 | 11656              | 2421          |
| Remote to local       | 995                | 2754          |
| Denial of services    | 45927              | 7456          |
| User to root          | 52                 | 200           |
| Total                 | 125973             | 22542         |

#### 3.2 Feature Scaling and Selection

There are 41 attributes in the NSL-KDD dataset. In this analysis, 14 common and basic characteristics, also known as traditional characteristics, are used.

#### 3.3 Conceptual Model Diagram

The proposed model consists of three sub modules. These are data preprocessing module, clustering and classification module with outlier detector and decision module. In the first module all the functionalities of data preprocessing such as feature selection, feature scaling, data encoding is performed. In the second module, data are cluster to the appropriate number of clusters with outlier detection. Thus, clustered data with outlier are then classified using Naïve Bayes classifier. The third module is a decision-making module.
3.4 Algorithm

Algorithm 1: Data Clustering

Input: Dataset
Output: K number of clusters with outlier
Initialization:
1. Randomly choose μ_1, Σ_1, π_1
2. Specify k
3. Choose an initial random gaussian parameter θ
4. E step
5. Compute P (Z_i = k |X_i, θ); P (X_i | Z_i = k, θ)
6. M step
7. Update gaussian parameters μ_1, Σ_1, π_1
8. if log-likelihood value converges
9. else
10. Compute ϒ_k
11. Update gaussian parameters μ_1, Σ_1, π_1
12. Assign data to appropriate cluster
13. End

3.5 Outlier Detection

Outlier detection is the method of detecting the pattern in data that did not expect property. Following is the process of outlier detection:

- Randomly choose data in the dataset and measure the distance of the data to all other data. If the distance between the data and certain data is below the radius that we already set, assign that certain data as a neighbor, then assign the data and its neighbors as 1 cluster.
- Do as in previous step but the data is replaced by its neighbors. Neighbors of the neighbor are in the same cluster with previous data. Do this step until all detected neighbor is chosen.
- When all detected neighbor is chosen, construct a new cluster using data that has not been chosen. The new clusters are formed as in steps first and second. The data that are not part of any cluster considered as an outlier.

Table 3.5 Outlier Statistics

| Outlier = TRUE | Outlier = FALSE |
|---------------|----------------|
| 32194         | 125973         |
| 25.55%        | 74.45%         |

3.6 Clustering

Clustering is a non-supervised approach to machine learning, but it can be used to maximize the precision of the supervised machine learning algorithm and cluster the data point into similar groups.

The purpose of clustering is to create dataset sub-population based on clustering results and to develop separate cluster classification models. Clustered membership can be considered as a feature in the classification and may have more details from these features. That improves the parallel processing capability of the model and manages data skews. That increases the accuracy of the classification.

3.6.1 EM Clustering

The expectation maximization (EM) clustering algorithm measures probabilities of cluster membership based on one or more distributions of probabilities. The goal of the clustering algorithm is then, given the (final) clusters, to maximize the overall likelihood or probability of the results.

Each gaussian j (j=1,2,...,k) is defined in the EM clustering by its own μ and σ^2 as:

\[ P(X | μ_j, σ_j^2) = N(X; μ_j, σ_j^2) = \frac{1}{(2πσ_j^2)^{d/2}} e^{-\frac{(x-μ)^2}{2σ_j^2}} \]  

Where,
- μ is mean
- σ is standard variable
- x - μ is the distance between two points.
- Each gaussian component has a mixture weight that indicates the likelihood.

3.7 Maximum Likelihood Estimation

In construction of a Bayesian classifier the class-conditional probability density functions need to be determined. The initial model selection can be done for example by visualizing the training data, but the adjustment of the model parameters requires some measure of goodness, i.e., how well the distribution fits the observed data. Data likelihood is such a goodness value. Assume that there is a set of independent samples X = \{X_i, . . . . . .X_n\} drawn from
a single distribution described by a probability density function \( P(x; \theta) \) where \( \theta \) is the PDF parameter list. The likelihood function can be written as:

\[
L(X; \theta) = \prod_{i=1}^{N} p(x_i; \theta)
\]

(2)

Equation (2) indicates the probability of \( X \) due to its distribution parameters \( \theta \). The goal is to calculate \( \hat{\theta} \) which optimize the likelihood.

\[
\hat{\theta} = \arg \max_{\theta} L(X; \theta)
\]

(3)

This function is generally not explicitly maximized, but rather the logarithm as:

\[
L(X; \theta) = \ln L(X; \theta) = \sum_{i=1}^{N} \ln p(x_i; \theta)
\]

(4)

This is due to easier to handle logarithm function analytically. The limit can be identified analytically according to \( P(x; \theta) \) by setting the derivatives of the log-like function to zero and \( \theta \) resolution. A gaussian PDF can be used which leads to the estimation of intuitive mean and variance but the research approach is generally intractable. In this case, the iterative method, such as the EM algorithm, is used in practice [1]. Maximizing the likelihood in certain situations will lead to unique estimates, which is the main issue of highest probability methods. The function of classifying vector in \( K \) classes is recalled by Gaussian mixture model. If different classes are treated as distinct (i.e., class samples don't say anything about other courses), the \( K \) class-conditional PDF estimation problem can be divided into \( K \) separate estimation problems.

### 3.8 Gaussian Mixture Probability Density Function

In a single dimensional bell-shaped curve, the Gaussian probability density function is defined by two parameters; mean (\( \mu \)) and variance (\( \sigma^2 \)). But, for \( D \) dimensional space it is in matrix form as:

\[
N(x; \mu, \Sigma) = \frac{1}{(2\pi)^{D/2} |\Sigma|^{1/2}} e^{-\frac{1}{2}(x-\mu)^\top \Sigma^{-1}(x-\mu)}
\]

(5)

Where,

- \( \Sigma \) is a matrix of covariance
- \( \mu \) is the mean vector.

Gaussian surfaces are \( \mu \)-centered hyperellipsoids.

The gaussian mixture model (GMM) consists of a mixture of several Gaussian distributions, thus representing different subclasses within a class. The probability density function is also known as the weighted sum of Gaussian.

\[
P(x; \theta) = \sum_{c=1}^{C} \alpha_c N(x; \mu_c, \Sigma_c)
\]

(6)

where

- \( \alpha_c \) is the component weight \( c \), \( 0 < \alpha_c < 1 \) for all components, and \( PC \ c=1 \)
- \( \alpha_c \) is the list of parameters whose value is equal to 1.
- \( \theta = \{\alpha_1, \mu_1, \Sigma_1, ..., \alpha_C, \mu_C, \Sigma_C\} \)

defines a fundamental Gaussian density.

### 3.9 Basic EM Estimation

Suppose, \( X \) is all good features of sample and \( Y \) is all unknown features of sample, then the expectation (E) step of the EM algorithm is

\[
Q(\theta; \theta^i) \equiv E_{Y \mid X} [ \ln L(X, Y; \theta) \mid X; \theta^i ]
\]

(8)

Where \( \theta^i \) is the previous distribution parameter estimate and \( \theta \) is the distribution-descriptive estimation variable for the new estimate. \( L \) is the probability function which determines the likelihood of the data, including the unknown attribute \( Y \) marginalized in relation to the current distribution estimate defined by \( \theta^i \). Maximization step (M) is to optimize \( Q \) for \( \theta \) and set steps are repeated until the conditions of convergence have been met.

\[
\theta^{i+1} \leftarrow \arg \max_{\theta} Q(\theta; \theta^i)
\]

(9)

It is proposed in [14] that the convergence parameters

\[
Q(\theta^{i+1}; \theta^i) - Q(\theta^i; \theta^{i+1}) \leq T
\]

(10)

with a correctly chosen \( T \) and in [13] that

\[
\|\theta^{i+1} - \theta^i\| \leq e
\]

(11)

The EM algorithm begins with an initial distribution parameter guess, which ensures that the log-likelihood will increase on each iteration up to converge. Convergence results in a local or global limit, but it can also lead to specific estimates, especially for Gaussian mixture distributions with arbitrary matrices. The definition and implementation of the general EM algorithm for the Gaussian mixture model can be found in [6,14]. One of the main problems of EM algorithm is to initialize. The selection of \( \theta \) defines where the algorithm converges or reaches the space parameter boundary that generates singular, insignificant results. Many solutions use random multiple starts or a clustering initialization algorithm [7]. The Gaussian mixtures implementation of the EM algo-
Algorithm as follows:

Let,

X is incomplete data
Y is knowledge of component that produced each sample X

For each \( X_n \), a binary vector is assigned as:

\[
y_n = \{ y_{n,1}, \ldots, y_{n,c} \}
\]

where,

\( y_{n,c} = 1 \), if component c or zero otherwise was generated in the sample.

The maximum probability of data log is

\[
\ln L(X, Y; \theta) = \sum_{n=1}^{N} \sum_{c=1}^{C} y_{n,c} \ln \left( \alpha_c \cdot p(x_n | c ; \theta) \right)
\]

The purpose of E step is to calculate conditional expectancy for the whole log-like data, Q-function is produced by X and \( \theta^i \) is current parameters estimation. As the whole data log-like function in L \((X, Y; \theta)\) is straightforward to the missing Y. Conditional expectation \( W \) simply needs to be determined and placed in \( \ln L(X, Y; \theta) \). That’s why

\[
Q(\theta, \theta^i) = E \ln L(X, Y; \theta) | X, \theta^i = \ln L(X, W; \theta)
\]

Where:

\( \omega_{n,c} \) elements have been defined as

\[
\omega_{n,c} = E [ y_{n,c} | X, \theta^i ] = \Pr[ y_{n,c} = 1 | x_n, \theta^i ]
\]

The estimate is determined using the Bayes law

\[
\omega_{n,c} = \frac{\alpha_c \cdot p(x_n | c ; \theta^i)}{\sum_{j=1}^{C} \alpha_j \cdot p(x_n | j ; \theta^i)}
\]

Where \( \alpha_c \) is the probability of a priori, and \( \omega_{n,c} \) is the likelihood of posteriori of \( Y_{n,c} = 1 \) after observing \( X_n \). In other words, “\( \omega_{n,c} \) is the probability that \( X_n \) was produced by component c”.[21]

If the M-step is used to evaluate the distribution parameters for C-component Gaussian mixture, with Arbitrary covariance matrices the following formulas will be used:

\[
\alpha_c^{i+1} = \frac{1}{N} \sum_{n=1}^{N} \omega_{n,c}
\]

\[
\mu_c^{i+1} = \frac{\sum_{n=1}^{N} x_n \omega_{n,c}}{\sum_{n=1}^{N} \omega_{n,c}}
\]

Table contains classification statistics, the number of instances transmitted into each cluster, and the proportion of instances from each cluster’s total data.

| Cluster | No. of instances | % of instances |
|---------|-----------------|---------------|
| 1       | 45108           | 36%           |
| 2       | 34025           | 27%           |
| 3       | 13432           | 11%           |
| 4       | 27394           | 22%           |
| 5       | 6013            | 5%            |

3.10 Classifier

A classifier may adjust a number of parameters to the function. This is known as training. The samples in the training are labelled in supervised learning and the training algorithm tries to reduce the training set’s classification error. Unsupervised learning does not label samples, but the training algorithm recognizes clusters and classes. The training samples are not also classified in reinforcement learning, but the training algorithm uses input to inform whether or not to identify a sample properly.[40]

3.10.1 Bayesian Classification

Bayesian classification and its decisions are based on the probability theory and on the idea that the most likely or lowest risk i.e, expected cost is chosen. Suppose there is a classification task in which to assign functional vectors to K various classes. A vector function is labelled with \( x = [X_1, X_2, \ldots, X_D] \) T. Where, D is the dimension of a vector. Probability that a feature vector \( x \) belongs to class \( \omega_k \) is \( p(\omega_k | x) \), and this is referred to as a posteriori
probability. The vector’s classification is based on the subsequent probabilities or decision risks determined from the probabilities. The conditional probability can be determined by Bayes formula as

\[
P(\omega_k | x) = \frac{P(x | \omega_k)P(\omega_k)}{P(x)}
\]  

(19)

where \( P(\omega_k | x) \) is the probability density function of class \( \omega_k \) in the feature space and \( P(\omega_k) \) is the a priori probability. That gives the likelihood class before any characteristics are calculated. When previous probabilities are not known, they can be calculated in the training set according to the class proportions.

\[
P(x) = \sum_{i=1}^{k} P\left(\frac{x}{\omega_i}\right)P(\omega_i)
\]  

(20)

It’s just a factor in scaling to ensure that later probabilities are actual probabilities, that is, their sum is 1. Choosing the lowest retrograde likelihood class will illustrate the minimum pliability of error \(^{[1,4]}\). However, if the costs of making various types of error are not consistent, a risk function can be used which calculates the expected cost with the following probabilities and selects the lesser-risk class. The main problem in the Bayesian classification is the class-conditional density function \( p\left(\frac{x}{\omega K}\right) \). The function defines the dispersion of feature vectors within a specific class, i.e., the class model. It is always unclear in reality, except for certain artificial classification activities. With a variety of methods, the distribution can be calculated in the training set.

3.11 Unit of Results

The model performance is calculated based on the following parameters and unit.

3.11.1 Accuracy of Classification

It is the proportion of correctly classified.

\[
\text{Classification accuracy} = \frac{TP}{(TP + TN + FP + FN)}
\]

3.11.2 Sensitivity (True Positive Fraction)

It is the percentage of the number of properly identified attack.

\[
\text{Sensitivity} = \frac{TP}{(TP + FN)}
\]

3.11.3 Specificity (True Negative Fraction)

It is the percentage properly categorized.

\[
\text{Specificity} = \frac{TN}{(TP + FN)}
\]

3.11.4 False Alarm Rate (FAR)

It is the percentage of the number of normal connections in correctly classified.

\[
\text{False alarm rate (FAR)} = \frac{FP}{(TN + FP)}
\]

3.11.5 Detection Rate (Precision)

It is the rate of detection of total anomaly from the total flow of packets in the network.

\[
\text{Detection rate (DR)} = \frac{TP}{(TP + FP)}
\]

Where,

- True positive (TP) = Attacks that are correctly detected as attack.
- True negative (TN) = Normal data that are correctly detected as normal.
- False positive (FP) = Normal data that are incorrectly detected as attack.
- False negative (FN) = Attack that are incorrectly detected as normal.

4. Results and Discussion

Based on obtained result, the overall accuracy in compared with different algorithms. The obtained result is illustrated in the following table.

Table 4. Result Comparison of Different Algorithm

| Attack Class | K-NN | C4.5 | SVM | DSSVM | K means with NB | Proposed method |
|--------------|------|------|-----|-------|----------------|-----------------|
| Normal       | 98.3 | 97.0 | 97.7| 98.4  | 74.11          | 97.48           |
| DoS          | 97.0 | 96.8 | 97.2| 97.2  | 86.05          | 81.65           |
| Probe        | 79.4 | 84.3 | 86.1| 87.5  | 92.48          | 97.13           |
| R2L          | 6.5  | 3.0  | 7.2 | 6.3   | 32.02          | 95.17           |
| U2R          | 11.8 | 4.4  | 9.2 | 3.1   | 19.0           | 73.66           |

From the above discussion, it is cleared that low frequency attack (probe, R2L, U2R) detection rate is improved in the integrated models. In proposed model this rate is significantly improved. Also, the detection rate for
normal class also improved in competitive ratio with the existing algorithms. 

Firstly, the overall accuracy of DoS can be improve. Next improvement can be done in reducing the computation time at outlier detection.

5. Conclusions

The research work observed with overall performance winner as integration of Expectation Maximization clustering with Naïve Bayes classifier for intrusion detection over Integration of K-Means clustering and Naïve Bayes classifier is considered to be best in terms of precision, sensitivity, specificity, and false alarm rate for the different types of attack class such as Probe, R2L, U2R and normal. It is shown that clustering plays a supportive role for classification by parallel computation so that the computation capacity of the model is improved. Since the whole dataset is clustered in a K number of clusters and compute parallelly, it can be used as real time/online computation with full efficiency computation on large data.

As the overall result of this model is significantly improved in different attack classes such normal, probe, R2L and U2R. But the other intrusion detection system has a higher detection rate for DoS attack.

Further improvement can be done in a number of ways.

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