ABSTRACT

In recent years some reactors have experienced significant steam dryer cracking. The cause of the dryer’s failure was considered as flow-induced acoustic resonance at the stub pipes of the safety relief valves (SRVs) on the main steam lines (MSLs). A research program was started to investigate the acoustic resonance of the steam dryer. Most studies used scaled down method, while our research based on the full scale steam dryer of the prototype CAP1400 but with only one unit of the steam dryer. The purpose of our research program is to study the strength of the steam dryer under flow-induced acoustic resonance. This paper introduces the parameter selection of the main pipe and the stub pipe through numerical method and theoretical method.

1. INTRODUCTION

In recent years some reactors have experienced significant steam dryer cracking. The detailed inspection of the stem dryer showed that it was likely that the steam dryer had been damaged by high cycle fatigue due to acoustic-induced vibration[1,2]. The cause of the dryer’s failure was considered as flow-induced acoustic resonance at the stub pipes of the safety relief valves (SRVs) on the main steam lines (MSLs). Acoustic resonance was considered to be generated by the interaction between the sound field and an unstable shear layer across the closed side branches of the SRV stub pipe (shown in Fig. 1), where the fluctuating pressure or sound was generated by unsteady motion of a vortex. And the resonance of the quarter wavelength mode is excited by the vortex sound in the SRV stub pipe[3].
The phenomenon of flow-induced acoustic resonance has been investigated by many researchers [3-10]. Most studies used scaled down method, while our research based on the full scale steam dryer of the prototype CAP1400 but with only one unit of the steam dryer. The purpose of our research program is to study the strength of the steam dryer under flow-induced acoustic resonance. The schematic diagram of the test facility is shown in Fig. 2. The test facility consists of a compressor, a gasholder, a test vessel, a steam dryer, a main pipe, a stub pipe, a stable section, a throatable nozzle, a super expansion section and a silencer. In order to get raise the sound power level (SPL) of the steam dryer to the highest, theoretically analysis was used to confirm the parameters of the test facility. This paper will introduce the parameter selection of the main pipe and the stub pipe through numerical method and theoretical method.

2. NUMERICAL ANALYSIS

Based on ANSYS, we study the effect of the aerodynamic noise on four parameters which are shown in Fig. 3 (the height of the stub pipe H, the velocity of the main pipe V, the length of the main pipe L and the diameter of the main pipe D). Figure 4 shows the position of the measuring points.

| Working condition | H (mm) | L (mm) | D (mm) | V (m/s) |
|-------------------|-------|-------|--------|--------|
| I                 | 240   | 3000  | 110    | 45     |
| II                | 185   | 3000  | 110    | 45     |
| III               | 65    | 3000  | 110    | 45     |

Fig. 5 Sound pressure frequency spectrum curve: a) p2; b) p5
The curve of SPL with frequency is shown in Fig. 5. At different measuring points, there is a strong monotonic noise. When the height of the stub pipe is much greater than the diameter of the stub pipe, the main peak frequency is about 310 ~ 330 Hz which is similar to the first-order modality of the stub pipe. When the height of the stub pipe is close to the diameter of the stub pipe, the main peak frequency is close to the second-order modality of the stub pipe.

![Fig. 6 SPL distribution map under different height of the stub pipe]

Figure 6 shows the distribution of SPL in the pipe under different height of the stub pipe. It can be seen that SPL increases as the height of stub pipe increases.

### 2.2 THE INFLUENCE OF THE LENGTH OF THE MAIN PIPE

In this case, three other parameters (the height of the stub pipe, the diameter of the main pipe and the velocity of the main pipe) were fixed and the length of the main pipe was changed to investigate its influence on SPL. The working conditions of the compared numerical example are shown in Table 2.

| Working condition | H (mm) | L (mm) | D (mm) | V (m/s) |
|-------------------|--------|--------|--------|---------|
| I                 | 240    | 3000   | 110    | 45      |
| II                | 240    | 2300   | 110    | 45      |

![Fig. 7 Sound pressure frequency spectrum curve: a) p2; b) p5]

In Fig.7 it can be seen that with the increase of the length of the main pipe, the peak frequency is almost the same, but the strength slightly decreases. Taking the calculation of the grid as well as the discrete error into account, the effect of the length changes of the main pipe on SPL can be ignored.

### 2.3 THE INFLUENCE OF THE DIAMETER OF THE MAIN PIPE

In this case, three other parameters (the height of the stub pipe, the length of the main pipe and the velocity of the main pipe) were fixed and the diameter of the main pipe was changed to investigate its influence on SPL. The working conditions of the compared numerical example are shown in Table 3.

| Working condition | H (mm) | L (mm) | D (mm) | V (m/s) |
|-------------------|--------|--------|--------|---------|
| I                 | 240    | 2300   | 110    | 45      |
| II                | 240    | 2300   | 110    | 45      |

![Fig. 7 Sound pressure frequency spectrum curve: a) p2; b) p5]

In Fig. 8 it can be seen that the change of the diameter of the main pipe has a significant influence on the flow field in
the pipe. With the increase of the diameter of the main pipe, the Y direction of spatial scales increase which makes the flow more intensely.

In Fig. 8 it can be found that the noise with the 110mm diameter appears obvious monotonic peak frequencies, while the noise of 220mm diameter is more like a broadband noise.

2.4 THE INFLUENCE OF THE VELOCITY OF THE MAIN PIPE

In this case, three other parameters (the diameter of the main pipe, the length of the main pipe and the height of the stub pipe) were fixed and the velocity of the main pipe was changed to investigate its influence on SPL. The working conditions of the compared numerical example are shown in Table 4.

| Working condition | H (mm) | L (mm) | D (mm) | V (m/s) |
|-------------------|-------|-------|--------|---------|
| I                 | 185   | 3000  | 110    | 30      |
| II                | 185   | 3000  | 110    | 45      |
| III               | 185   | 3000  | 110    | 60      |
| IV                | 185   | 3000  | 110    | 75      |
| V                 | 185   | 3000  | 110    | 90      |

In Fig. 9 it can be seen that under the condition of low

Fig. 9 Sound pressure frequency spectrum curve: a) p2; b) p5

Fig. 10 Sound pressure frequency spectrum curve: a) p2; b) p5

In Fig. 10 it can be seen that under the condition of low
velocity (30 m/s), the resonant noise could not be excited either in the main pipe or in the stub pipe.

With the increase of the flow rate, the level of the noise begins to increase first, and in certain speed range (60 m/s ~ 75 m/s) it can reach the maximum value. However, with the continuous increase of the flow rate, the noise then intensity decreases after the peak value. In the calculation of the speed range, the noise shows monotonic frequency characteristic, the peak frequency moves to the high frequency band with the increase of flow rate, which is basically the same as the change of modal frequency characteristics. The peak frequencies were 325 Hz (45 m/s), 375 Hz (60 m/s), 395 Hz (75 m/s) and 450 Hz (90 m/s) respectively.

The curve of SPL changed with flow rate at P2 and P5 are shown in Fig. 11. Low velocity (30m/s) fails to excite the resonant noise, and the SPL at the measured point P2 is almost the same as the measuring point P5. While the SPL at the measuring point P5 is larger than that at the measuring point P2 under other flow velocity. Total SPL with the velocity variation is not linear, it first increases with the speed, and when it reaches its maximum value, it decreases gradually with the increasing speed.

3. THEORETICAL ANALYSIS

In this part the theoretical model and numerical calculation results were combined to analyze acoustic noise propagation.

3.1 MATHEMATICAL MODEL OF NOISE PROPAGATION

Based on the numerical simulation results, combined with the theory of sound propagation, it can be formed the following mathematical model.

There is one assumption that the acoustic wave propagated in the form of plane wave.

Based on the general complex solution of wave equation, the general form of the incident wave and the reflected wave can be expressed as:

Incident wave:
\[ p_i = p_{ia} e^{i(\omega t - kx)} \]  

Reflected wave:
\[ p_r = p_{ra} e^{i(\omega t + kx + \varphi)} \]  

Where \( p \) is Amplitude, \( \varphi \) is the phase difference produced by reflection.

The sound pressure reflection coefficient as the ratio of the reflected wave to the incident wave can be defined by:
\[ r_p = \left| \frac{p_r}{p_i} \right|_{x=0} = \left| \frac{p_{ra}}{p_{ia}} \right| e^{i\varphi} \]  

So, the amplitude ratio before and after reflection can be used to define the acoustic pressure amplitude reflection coefficient:
\[ \left| p_p \right| = \frac{p_{ra}}{p_{ia}} \]  

The total sound pressure can be expressed as:
\[ p_a = p_i + p_r = p_{ia} e^{i(\omega t - kx)} \left( 1 + \left| r_p \right| e^{i(2kx + \varphi)} \right) \]  

The amplitude is:
\[ \left| p_a \right| = p_{ia} \sqrt{1 + \left| r_p \right|^2 + 2 \left| r_p \right| \cos(2kx + \varphi)} \]  

if \( 2kx + \varphi = \pm 2n\pi \), \( \left| p_a \right|_{\text{max}} = p_{ia} + p_{ra} \)

if \( 2kx + \varphi = \pm (2n + 1)\pi \), \( \left| p_a \right|_{\text{min}} = p_{ia} - p_{ra} \)

Therefore, the acoustic wave is the linear superposition of the incident wave and the reflected wave, and the standing wave effect will occur.

3.2 MODEL NUMERICAL VERIFICATION

Fig.12 ~ Fig.14 show the distribution of SPL under different length of the main pipe (3000 mm vs. 2300 mm) and different velocity of main pipe (45 m/s vs. 60 m/s). The right graphs in Fig.12 ~ Fig.14 show the distribution of SPL with the length of the main pipe. It can be found that there was standing wave effect on upstream direction.

Fig.12 Distribution of SPL (L = 3000mm, V = 45 m/s)
Fig.13 Distribution of SPL (L = 3000mm, V = 60 m/s)
Fig.14 Distribution of SPL (L =2300mm, V = 60 m/s)
Based on the mathematical model, the wavelength of standing wave can be calculated, and the result can be compared with numerical result. Using the formula (6), when the peak wavelength was satisfied, the following formula was established:

\[ 2k\Delta x = 2\pi, \quad k = 2\pi/\lambda \]  

So the wavelength of standing wave is:

\[ \Delta x = \lambda/2 \]  

Using equation (8) it can be solved that the wavelength of standing wave under the frequency is about 325 Hz. Therefore, the wavelength under the frequency is:

\[ \lambda = \frac{340}{325} = 1.05 \text{ m} \]  

Using equation (8) it can be solved that the wavelength of standing wave under the frequency is 0.525 m which is almost the same as the numerical result.

When the flow velocity is 60 m/s, the main peak frequency was obtained about 375 Hz by the numerical simulation. Using formula (8) it can be obtained that the wavelength of standing wave by theoretical model is 0.453 m which is almost the same as the numerical result 0.432 m.

Based on the theoretical model, it can be found that the spread of noise in the upstream of the main pipe has the following rules: the anterior length of the main pipe does not affect the maximum SPL, but due to the presence of standing wave effect, it affected the distribution of sound pressure in the upstream of the main pipe.

4. CONCLUSIONS

This paper combined with theoretical modeling and numerical simulation analysis to investigate the generation mechanism and propagation characteristics of aerodynamic noise. The main conclusions were as follows:

- The effect of the height of the stub pipe on the peak frequency is not obvious, but SPL increases as the height of stub pipe increases.
- The noise with 110mm diameter appears obvious monotonic peak frequencies, while the noise of 220mm diameter is more like a broadband noise.
- The effect of the length changes of the main pipe on SPL can be ignored.
- The total SPL with the velocity variation is not linear. It first increases with the increasing speed, and when it reaches the maximum value, it decreases gradually with the increasing speed.
- The interaction between the air flow of the main pipe and the stub pipe will produce obvious monotonic frequency noise. The noise is propagated upstream in the form of plane wave which makes the standing wave effect. The anterior length of the main pipe does not affect the maximum SPL, but due to the presence of standing wave effect, it affected the distribution of sound pressure in the upstream of the main pipe.

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