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Global modelling study (GSM TIP) of the ionospheric effects of excited $N_2$, convection and heat fluxes by comparison with EISCAT and satellite data for 31 July 1990

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Abstract. Near-earth plasma parameters were calculated using a global numerical self-consistent and time-dependent model of the thermosphere, ionosphere and plasmosphere (GSM TIP). The model results are compared with experimental data of different origin, mainly EISCAT measurements and simultaneous satellite data ($N_e$ and ion composition). Model runs with varying inputs of auroral FAC distributions, temperature of vibrationally excited nitrogen and photoelectron energy escape fluxes are used to make adjustments to the observations. The satellite data are obtained onboard Active and its subsatellite Magion—2 when they passed nearby the EISCAT station around 0325 and 1540 UT on 31 July 1990 at a height of about 2000 and 2200 km, respectively. A strong geomagnetic disturbance was observed two days before the period under study. Numerical calculations were performed with consideration of vibrationally excited nitrogen molecules for high solar-activity conditions. The results show good agreement between the incoherent-scatter radar measurements ($N_e$, $T_e$, $T_i$) and model calculations, taking into account the excited molecular nitrogen reaction rates. The comparison of model results of the thermospheric neutral wind shows finally a good agreement with the HWM93 empirical wind model.

1 Introduction

Global self-consistent models of the Earth’s upper atmosphere, ionosphere, plasmasphere and magnetosphere including electrodynamics have been developed during the last decade to describe the complex physical processes of the near-Earth plasma environment as a whole. Since the development of theoretical and semi-empirical models describing the spatial-temporal behaviour of individual regions of near-Earth space (e.g. thermospheric composition models or mid-latitude ionospheric models), there has been a progression from ‘single-sphere models’ to combined models which account for the complexity of the processes, the availability of a rich amount of different data and for the progress in numerical technique. Large-scale electrodynamics play an important role in the neutral and plasma dynamics of the upper atmosphere and in its interplay with the plasmasphere and magnetosphere. Several global models have been developed which take care of the complex coupled nature of near-Earth space (Fuller-Rowell et al., 1987; Namgaladze et al., 1988; Richmond et al., 1992; Roble and Ridley, 1994; Moffett et al., 1996).

One of these models, the GSM TIP (Global Self-consistent Model of the Thermosphere, Ionosphere and Plasmosphere), was developed at the West Department of IZMIRAN (former Kaliningrad Observatory) and modified later at the Polar Geophysical Institute in Murmansk (Namgaladze et al., 1990, 1991); it is this model which serves as basic tool for the present study. Similar models are the TIE GCM (Thermosphere-Ionosphere-Electrodynamics General Circulation Model) and the TIME GCM (further development including the Mesosphere) from the National Center for Atmospheric Research (NCAR) in Boulder and the CTIPM (Coupled Thermosphere, Ionosphere, and Plasmasphere Model) from the University of Sheffield and the University College, London. However, the CTIPM uses magnetospheric and E-layer dynamo electric fields as external input parameters only (Moffett et al., 1996), while the NCAR models do not explicitly calculate the plasmasphere and magnetosphere but specify upper-boundary plasma fluxes at 500 km (Richmond et al., 1992; Roble and Ridley, 1994).

The GSM TIP was already presented during the last EISCAT workshop in Andenes with an application to the event of 24–25 March 1987 (Namgaladze et al., 1996). In the present paper, we investigate an interval during summer solstice high solar-activity conditions using data from the EISCAT facility as well as satellite data from the Active mission. Satellite data cover large space regions...
with latitudinal profiles along the orbital track for selected
time-moments only, while the incoherent-scatter radar
provides plasma parameters of the upper atmosphere for
longer time-intervals with good time resolution in a lim-
ited region of space. Therefore, the task of combining
simultaneous satellite and radar measurements within
a common global numerical model can give some insights
into the complex physical coupling processes.

2 EISCAT and satellite data for 31 July 1990

The UHF system of the EISCAT radar facility allows
three-dimensional measurements of ionospheric para-
eters such as electron density $N_e$, electron temperature
$T_e$, ion temperature $T_i$, ion drift $V_i$, and ion composition
at the heights of the E-, F- and F-layers up to upper
ionospheric altitudes of about 600 km. We used the Com-
mon Program 1, version I (CP-1-I), registrations from the
time-interval 1900 UT 30 July till 0400 UT 01 August
1990, and directed our attention mainly to data taken on
day number 212 (31 July 1990) for intercomparison with
satellite data from the Active mission. The CP-1 config-
uration is intended to provide measurements along the
magnetic field line above the Tromsø station (with an
inclination of about 77.6° for the flux tube with the Mc-
Ilwain parameter $\lambda = 6.46$). For this purpose the Tromsø
antenna is kept fixed parallel to the magnetic field at
278.5-km altitude and the remote sites take measurements
in a 5-min cycle, providing a three-dimensional pattern of
the drift velocity in the F region.

The Active mission was launched on 28 September
1989 into a near polar orbit with an inclination of about
82.5°, a perigee of 500 km and an apogee of 2500 km. It
consisted of the main satellite Active and the small Czech
subsatellite Magion-2, which is able to be stirred, for
diagnosis purposes. On 31 July the satellite pair passed
nearby the EISCAT radar station during orbit numbers
3805 at 0325 UT and 3812 at 1540 UT. Real-time tele-
metry was used so that measurements during overflights
above Europe are available. Depending on satellite height
these time-series have durations of 15 to 35 min and cover
a latitudinal range from about 20° to 80°.

The Czech-Russian ion mass spectrometer HAM-5
(Afonin et al., 1994) used for this study was placed on
board the main satellite. It is a three-stage Bennett ana-
lyser with electron multiplier operating in the current
mode on its output which uses the modulation mode for
removing the base flux. The potential of the analyser was
floating and controlled by the potential of an isolated
probe located near the aperture of the analyser. The mass
spectrometer had discrete ranges around the masses 1, 2, 3
and 4, and a continuous range from 6 to 64 amu, all with
a constant accelerating voltage and frequency sweep. The
mass resolution $M/\Delta M$ (on the level of 10 per cent) was 25.
So, concentrations of O+, N+, He+, H+ and O2+, as well
as of molecular ions (at lower altitudes), were obtained
along the satellite orbit with a time resolution of about 6 s.

The Langmuir probe on-board the subsatellite
Magion-2 working in the sweep adaptive voltage regime
performs in situ diagnoses of the cold thermal plasma in
the topside ionosphere. It is a cylindrical probe oriented
parallel to the geomagnetic field lines, thus it measured
mainly field-perpendicular plasma parameters, namely the
electron density $N_e$, electron temperature $T_e$ and the effec-
tive ion mass. The errors of $N_e$ measurements are esti-
mated to be less than 10 per cent. The time resolution of
the Langmuir-probe measurements along the orbital trace
used throughout this paper is 2 s.

3 Geophysical conditions

The period under study is generally characterized by high
solar activity near the maximum of the 22nd solar cycle
with average values of $F_{10.7}$ solar radiation around 200.
We selected a time-interval near the northern summer solstice
when EISCAT observations and satellite passages
over the radar station were available. This took place on
the third day of the recovery phase of a geomagnetic
storm (with peak values of $K_p = 8\)$. The observed $A_p$,
$K_p$ and $D_s$ indices for the period 24 July–2 August 1990
are shown in Fig. 1. The onset of a moderate geomagnetic

![Fig. 1. Geophysical conditions during the time-interval under study](image-url)
storm was recorded with two sudden storm commencements (SSC) at 0108 and 0331 UT on 28 July with a minimum $D_s$ value of 129 nT at 0400 UT on 29 July 1990. During the night of 28–29 July the three-hourly $Ap$ index reached peak values of 170, but on 31 July these values returned to a quiet-time level around 4 and $K_p$ went down to values between 0+ and 2+. (see Fig. 1).

In addition, $f_r F_2$ data from some European ground-based ionosonde stations (Rome, Juliusruh/Rügen, St. Peter Ording, Kaliningrad, Kiew, Loparskaya) were used to obtain a more comprehensive pattern of the geophysical situation. The $f_r F_2$ values of 31 July from all these stations are near the median values, after some days with strong negative ionospheric storm effects (not shown here). So, one may assume that the ionospheric conditions on 31 July 1990 recovered from the moderate geomagnetic storm two days before.

4 The model GSM TIP

GSM TIP has been described in detail by Namgaladze et al. (1988, 1990, 1991). It comprises several computational blocks for the description of the thermosphere, ionosphere, plasmasphere and near-Earth magnetosphere in a height range from 80 km to 15 Earth radii including electromagnetic coupling processes as a single system.

For a given set of input data (possibly time-dependent), the GSM TIP model calculates the time-dependent global three-dimensional structure of the neutral gas temperature $T_n$, mass density, wind velocity vector $V_0$ and number density of the main neutral gas components $N_2$, $O_2$ and $O$ for the height range 80–520 km by means of numerical integration of the corresponding three-dimensional continuity, momentum and heat balance equations in a spherical geomagnetic coordinate system. To reduce the computational efforts, an empirical thermospheric model, such as MSIS-86 (Hedin, 1987), can be used for the calculation of the thermospheric parameters as well, solving only the neutral-gas momentum equation to obtain its three-dimensional global circulation. It has been shown by Namgaladze et al. (1994) that the results of self-consistent GSM TIP model runs and GSM TIP modelling with the inclusion of the MSIS-86 model are comparable in a qualitative manner. A quantitative agreement has been stated there for mid-latitudes and quiet geomagnetic conditions only.

In the lower ionosphere model block the parameters of the E and F1 ionospheric regions are calculated, namely, the total concentration of the molecular ions $n(XY^+)$ = $n(NO^+)$ + $n(O_2^+)$ + $n(N_2^+)$, the ion and electron temperatures $T_i$ and $T_e$ and the molecular ion velocity $V(XY^+)$ neglecting heat and mass transfer terms. These equations are solved in the same coordinate system as the thermospheric block for the height range 80–520 km with the exception of the electron-energy equation, for which the upper boundary is fixed at an altitude of 175 km. These equations are first order in time only, so they require initial values but no boundary conditions.

In the ionospheric-protonospheric module, parameters of the F2 region of the ionosphere and of the plasmasphere are calculated, namely, the atomic-oxygen and hydrogen-ion number densities $n(O^\text{\textsuperscript{-}})$ and $n(H^\text{\textsuperscript{+}})$, as well as $T_i$ and $T_e$, ion velocities $V(O^\text{\textsuperscript{-}})$ and $V(H^\text{\textsuperscript{+}})$ for the height range from 175 km to the radial distance of 15 $R_e$. We assume that field lines with $L > 15$ (L parameter of McIlwain) are open. The plasma drift caused by crossed electric and magnetic fields is taken into account. The integration of the continuity, momentum and heat balance equations for the atomic ions is performed along dipole geomagnetic field lines in a magnetic dipole coordinate system.

The equation for the potential of the electric field $E = -\nabla(\phi)$ is solved in the fourth program module including the dynamo action of the thermospheric winds and magnetospheric sources via the auroral field-aligned current system (FACs). The spherical geomagnetic system is used in this block.

The spatial steps of the numerical integration are $10^\circ$ in geomagnetic latitude for the thermospheric and lower-ionospheric modules, $5^\circ$ for the ionospheric-protonospheric and electrical-potential modules, and $15^\circ$ in the geomagnetic longitude for all groups of the model equations. In the vertical direction the thermospheric code uses 30 non-equidistant grid points between 80- and 520-km altitude which are distributed with step sizes increasing with a geometric progression roughly between 3 and 45 km from the bottom to the top. The ionospheric-protonospheric module (F2 region and plasmasphere) also has variable spatial steps along the magnetic field lines, with step sizes of about 15 km at the lower boundary at 175-km altitude up to several thousand kilometres near the apex of the flux tubes depending on the $L$ value up to a maximum distance of 15 Earth radii. The maximum number of grid points along a given field line is 140. The time integration step is 5 min.

In order to simulate the thermosphere-ionosphere parameters, the GSM TIP requires the following inputs: solar UV and EUV spectra, FACs connecting the ionosphere with the magnetosphere, and ionizing particle precipitation patterns and intensities.

Because there are no measurements of the solar EUV fluxes during the year 1990, we have used the technique of Nusinov (1984); it uses a non-linear scaling of the main solar spectral line intensities with the daily and the 81-day averages of $F_{10.7}$. The variations of the EUV flux observed by the AE-E satellite in 1977–1980 were used for this flux–model. Solar UV fluxes are as the Mount and Rottman (1983) data.

The ionospheric polar-cap convection pattern is controlled by the specific FAC distribution. Region-I and -II FACs (Iijima and Potemra, 1976) in the auroral zone are fixed at constant geomagnetic latitudes of 75° and 65°, respectively. They have been assumed with maximum densities of $2 \times 10^{-7}$ m$^{-2}$ for region-I and $5 \times 10^{-8}$ m$^{-2}$ for region-II currents, which are reached in the 06-18-MLT meridional plane under usual, non-storm conditions.

The electron precipitation patterns in the auroral zone (65°–75° geomagnetic latitude) have been assumed in the following simple form according to precipitation measurements typical for average geomagnetic-activity conditions
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5 Numerical results of modelling

In this study we confine ourselves to comparisons between model results and observations for two selected time-spans around 0325 and 1540 UT when the satellite pair passed nearby the EISCAT station during their orbits 3805 and 3812, respectively. We investigated in particular the sensitivity of model results to changes of the currently worst-known model input parameters: the temperature, \( T_e \), of the vibrationally excited molecular nitrogen \( \text{N}_2^* \), the ionospheric convection patterns driven by FACs and the suprathermal or photoelectron escape energy fluxes into the plasmasphere providing thermal electron heating fluxes from the plasmasphere into the ionosphere. The present knowledge about these input parameters is not precise enough, so that one can speculate about their values within reasonable limits in order to guess their effect by comparison with the measurements. These model runs were performed using the MSIS-86 neutral atmosphere model within the thermospheric computational block.

5.1 Early-morning calculations, orbit 3805

This subsection describes model results for 0325 UT when the Active satellite pair, during orbit 3805, crossed Central Europe near the EISCAT station. The values of observation are indicated by triangles throughout all the following figures, which compare EISCAT-measured profiles with modelling results. We used the EISCAT standard 5-min post-integrated parameter fit and produced median values of \( N_e \) and \( T_e \) profiles using 12 consecutive standard 5-min intervals around the time of overflight. The mean square deviations of the observed parameters are generally within the size of the used symbol (triangles).

Figure 2a–c demonstrates the effect of varying \( T_e \), on electron density (a) and electron- (b) and ion-temperature (c) profiles above the EISCAT station. The maximum photoelectron escape energy flux is set to \( 6 \times 10^{10} \text{ eV cm}^{-2} \text{s}^{-1} \) and the maximum FAC densities are assumed to occur in the 06–18-MLT meridians. The curves indicated by crosses present the model run where \( \text{N}_2^* \) has not been taken into account at all, while the other two cases show results with enhanced vibrational excitation of \( \text{N}_2^* \). The curves marked with asterisks show the case with vibrational temperature \( T_v = 1.25 T_n \) and the curves marked with squares for \( T_v = 1.5 T_n \). From Fig. 2 it is clear that the introduction of \( \text{N}_2^* \) reduces the \( N_e \), \( F_2 \)-peak density dramatically. Comparing the case of \( T_v = 1.25 T_n \) with the case of ignored \( \text{N}_2^* \), the \( F_2 \)-peak density is reduced by a factor of two. At the same time the electron temperature increases by about 900 K near the \( F_2 \) maximum at an altitude of 400 km. A further increase in vibrational temperature \( (T_v = 1.5 T_n) \) produces more dramatic changes.

The ion-temperature profiles are close to each other for all cases, especially below 450 km; there the agreement with the EISCAT data is quite good. Above that altitude level the different cases show some small variation and the modelled \( T_i \) begin to deviate from the observed values. This small discrepancy of about 200 K could be caused by insufficient Joule heating, but more likely by adiabatic cooling at high altitude (above 1500 km) due to large plasma escape velocities along the flux tubes in the model results. The high parallel thermal conductivity then results in lower \( T_i \) values down to about 500-km altitude.

The effects of different convection patterns on the local \( N_e, T_e \) and \( T_i \) profiles above the EISCAT station are shown in Fig. 3a–c. As before, the maximum photoelectron escape energy flux is set to \( 6 \times 10^{10} \text{ eV cm}^{-2} \text{s}^{-1} \) and model runs with \( T_e = 1.25 T_n \) are used. We compare different convection patterns which are produced by FAC
distributions with maximum densities in different meridional sectors. Curves marked by squares show the case where the maximum FACs are reached at 10–22 MLT, while curves with crosses stand for the other extreme with maximum FACs in the 06–18-MLT meridians; curves indicated by asterisks show the intermediate case, i.e. maximum FACs at 08-20 MLT. We see that a clockwise rotation of the maximum FACs from 10–22 to 08–20 MLT leads to a decrease in $N_e$ density and an increase in $T_e$, but a further clockwise rotation toward maximum FACs at 06–18 MLT reverses the process and results in an opposite behaviour in the vertical profiles of $N_e$ and $T_e$. As one may notice in Fig. 3c, the ion-temperature profiles are similar to the profiles of Fig. 2c below 450 km, but show variations of several hundred degrees above 600 km. These variations are determined in the same way as just shown, by the influence of adiabatic cooling at high altitude due to large parallel escape fluxes.

Figure 4a–c illustrates the effects of varying photoelectron escape energy fluxes on the $N_e$, $T_e$ and $T_i$ profiles above the EISCAT station. Again, the temperature of excited $N_e^+$ was assumed as $T_e = 1.25T_n$, and the maximum FACs occurred at the 08–20-MLT meridians for these model runs. It can be seen that an increase in the photoelectron escape energy flux from $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ (curves with crosses) to $10 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ (squares) leads to a decrease in the electron density mainly in the upper ionosphere and an increase in $T_e$ at the same heights. From the lower panel ($T_i$ in Fig. 4c) it is clear that the adiabatic cooling effects are even larger than in the previous case (Fig. 3c) due to faster escape velocities.

Results from the modelling studies detailed here were also compared with data from the Active satellite orbit 3805 (Figs. 5–7) for upper ionosphere parameters in a latitudinal range from 70° to 45°. The effect of enhanced $N_e^+$ temperatures on the latitudinal distribution of $O^+$ and $H^+$ is shown in Fig. 5. It can be seen that the $O^+$ concentration decreases by a factor of two and the
H\(^+\) density decreases by a factor of 3–4 in the latitudinal range between 70° and 65° if N\(_2^*\) processes with enhanced \(T_v\) are included. The effect is smaller at mid-latitudes.

The influence of different convection patterns on the distribution of O\(^+\) and H\(^+\) densities along orbit 3805 (Fig. 6) is similar to that shown in Fig. 3 as far as it concerns oxygen ions. Proton distributions are more sensitive to the rotation of the FAC patterns and reach a factor of 5 at the latitude of the EISCAT station. The drift pattern influence has a negligible effect at mid-latitudes.

Finally, the ion distributions along the satellite orbit 3805 for various photoelectron escape energy fluxes are shown in Fig. 7. It is clear that the atomic-ion distributions are not sensitive to changes of this input parameter at these latitudes.

5.2 Afternoon calculations, orbit 3812

In this section we present the corresponding numerical results of modelling for the time-span near 1540 UT, when the satellites passed over the EISCAT station during their orbit 3812. Since the effects of vibrationally excited N\(_2^*\) are almost identical to the effects at 0325 UT in the morning sector, as presented in Figs. 2 and 5, we concentrate here...
on the effects of convection and plasmaspheric heating fluxes.

Figure 8a–c compares the observed and calculated $N_e$, $T_e$ and $T_i$ profiles above the EISCAT station for different patterns of convection for the same cases as in Fig. 3 and with the same assumptions about the photoelectron escape energy flux and $T_e$. The clockwise rotation of the maximum FACs from 10–22 MLT to 06–18 MLT causes a steady decrease in $N_e$ and an increase in $T_e$ in accordance with the degree of rotation. It should be noted that for these cases $N_e$ and $T_e$ vary monotonically in contrast to the convection effects in the early-morning sector.

The effect of increasing photoelectron escape energy fluxes on the electron density profiles above EISCAT for the afternoon overflight around 1540 UT is shown in Fig. 9a to be relatively small. In contrast, the electron temperature reacts sensitively to the enhanced heating fluxes from the plasmasphere due to increased photoelectron escape energy fluxes (Fig. 9b). The agreement between measured and modelled ion temperatures is very good for all cases during the afternoon (cf. Figs. 8c and 9c).

Changes to the convection and photoelectron escape energy fluxes also have small effects on the ion distributions along satellite orbit number 3812 at low and mid-latitudes. Therefore, we show only the influence of excited $N_2^*$ on the electron-density distribution along the satellite orbit in Fig. 10. For this case the maximum FACs were in the 06–18 MLT meridional plane and the photoelectron escape energy flux was set to $2 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ for all latitudes except along the flux tube above the EISCAT station, where a value of $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ was assumed. It can be seen that the effect of vibrationally excited $N_2^*$ is different at different latitudes and its effect has an upper limit of a factor of 1.5.

6 Discussion

In the previous section we presented numerical model results obtained with the inclusion of the MSIS-86 neutral-atmosphere model and compared them with observations from EISCAT for two different local times (dawn and dusk) and with satellite data from the same time-spans but obtained over a certain latitudinal range. Since not all of the input model parameters can be determined correctly from experimental data, we have chosen three essential parameters, such as enhanced $N_2^*$ temperature $T_{v'}$, photoelectron escape energy fluxes and maximum FAC locations, to adjust their values accordingly to bring model results and measurements into agreement. We showed that the effect of introducing enhanced $N_2^*$ on the modelled vertical $N_e$ and $T_e$ profiles above EISCAT are very large for both dawn (0325 UT, Fig. 2) and dusk (1540
As in Fig. 8, but showing the influence of varying photo-electron escape energy fluxes with maximum values of $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ (curves with crosses), $7 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ (asterisks) and $10 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ (squares).

As in Fig. 5, for comparison of model results with measured electron density values obtained on-board Magion-2 (Langmuir probe) along the satellite orbit 3812. The effect of vibrationally excited N$_2^*$ is investigated: without N$_2^*$ (curves with crosses), assuming $T_e = 1.25T_n$ (asterisks) and $T_e = 1.5T_n$ (squares).

UT) sectors. The decreases in N$_e$ density at F2-peak altitudes varies from a factor of 2 in the dawn sector to a factor of 3 in the post-noon sector. In these cases, lower $T_e$ values correspond to higher N$_e$, and vice versa. A temperature difference of more than 1000 K is predicted at 400-km altitude between the case of absent N$_2^*$ and the other extreme (including N$_2^*$ with $T_e = 1.5T_n$). This result agrees with the model results of Ennis et al. (1995) for maximum solar activity in summer at mid-latitudes.

The convection electric fields have an important effect on ionospheric parameters at high latitudes, but the correct inclusion of this effect requires knowledge of the plasma convection over the entire high-latitude region. Unfortunately, we have no complete experimental data about the convection during this period of interest, since data from EISCAT radar alone are insufficient to determine the electric field over the entire high-latitude region; Rasmussen et al. (1986) have been faced with the same problem. Therefore, we varied the normal position of the maximum FACs (06–18 MLT) by rotating the meridional plane of maximum currents to calculate the electric-field distribution of ionospheric convection in the high-latitude region. In all these cases the model results have shown a two-cell convection with anti-sunward flow over the polar cap and return flow at lower latitudes (Fig. 11a–c). The cross-polar-cap potential drop varies weakly between 22.5 kV (Fig. 11b), 25.0 kV (Fig. 11a) and 27.5 kV (Fig. 11c). But at the same time the cross-polar electric field vector points in different directions: approximately from 04 to 16 MLT in the first case (a), 06–18 MLT in the second (b) and nearly 09–21 MLT in the last case (c). The effects of the rotated convection patterns on N$_e$ and $T_e$ are different for the dawn and dusk sectors, but generally smaller than the effects of vibrationally excited N$_2^*$. The changes in N$_e$ due to different convection patterns above EISCAT are about 50% near the F2 peak and about 600–700 K for $T_e$. As can be seen in Fig. 3a, the model gives remarkably good agreement between N$_e$ profiles above EISCAT and model results in the dawn sector when the maximum FACs are in the 10–22-MLT meridional plane and equally good agreement in the dusk sector when the maximum FACs are in the 08–20-MLT plane (Fig. 8a). However, the $T_e$ values are lower than EISCAT measurements in both cases.

Figure 12a–c show the eastward and northward components of the modelled electric field (left panels) and a comparison between the calculated meridional neutral wind with the corresponding values from the empirical HWM93 model for all three different convection patterns (a–c), adopted in our study. It can be seen that the clockwise rotation of the maximum FACs from 10–22 MLT to 06–18 MLT leads to a variation of the maximum values of both electric-field components and to slight changes of the meridional neutral-wind component. We use this figure
Fig. 11a–c. Electric-field-potential (kV) distribution at the northern hemisphere in a geomagnetic latitude/longitude frame with orthographic projection for three different FAC patterns: a maximum FACs in the 06–18-MLT, b 08–20-MLT c and 10–22-MLT meridional plane. The location of the EISCAT station for the two different time-moments is indicated by triangles.

for an explanation of the behaviour of the vertical $N_e$ profiles presented in Figs. 3 and 8 from the previous sections.

As we saw in Fig. 3, the rotation of the maximum FACs causes a non-regular behaviour of the $N_e$ profiles over EISCAT. The effect can be explained by the non-regular variations of the northward electric field component $E_n$ (west-east drift). We see that $E_n$ changes from $-7 \text{ mV m}^{-1}$ for the case with FACs maximum in the 10–22-MLT plane (case c) to $-9 \text{ mV m}^{-1}$ in the 08–20-MLT case (b) and $-8 \text{ mV m}^{-1}$ in the 06–18-MLT case (a, cf. Fig. 12). So, $E_n$ has its maximal negative value in the dawn sector for case b with FACs maximum in the 08–20 MLT plane and hence during the maximal zonal plasma drift from the night sector towards the morning sector.

The meridional wind (positive southward) contributes to an uplifting of the F2 layer, especially for the cases b and c (maximum FACs from 8–20 to 10–22 MLT).

During the overflights in the dusk sector (1540 UT), the meridional neutral wind component is near zero and the behaviour of the F2-peak electron concentration is determined by the electric-field components only. As we saw in Fig. 8, the $N_e$ concentration and the height of the F2-layer increase with the rotation of the maximum FACs from the 6–18-MLT plane to 10–22 MLT. This is caused by the eastward electric-field component $E_e$, which varies around 1540 UT from $-3 \text{ mV m}^{-1}$ to $+3 \text{ mV m}^{-1}$ for the different cases. The eastward electric-field component causes a meridional plasma drift, and hence acts to push ions up (as in case c) or down (case a) along the magnetic
field lines towards regions of lower or higher chemical loss rates, respectively. The zonal plasma drift ($E_n$) does not change its direction in all these cases.

An inspection of the right panels of Fig. 12a–c shows that the agreement between the modelled meridional wind velocities and the corresponding values from the HWM93 empirical wind model is quite good. This is valid especially near the time-moments of our interest in the dawn and dusk sectors.

The influence of the electron heating flux on upper ionospheric parameters, simulated in this study by the specification of the photoelectron escape energy fluxes, is more pronounced during dawn than in the dusk sector. In the dusk sector, as seen in Fig. 9a (1540 UT), the model variability of $N_e$ profiles is only around 20%, while the photoelectron escape energy fluxes vary from $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ to $10 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$. But in the same time $T_e$ increases appreciably from 2500 to 3200 K at 400-km altitude (Fig. 9b). Figure 9a reveals also, that the model $N_e$ concentrations reproduce the observed vertical profiles above about 350 km (at least for the case with a flux of $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$), but underestimate the electron density below this altitude. An increasing heating flux results in only a small decrease of the $N_e$ density above 350 km, and has practically no influence below this level.

In the dawn sector, as seen in Fig. 4a for 0325 UT, the model $N_e$ concentration appreciably underestimates the electron density above 250 km. This difference becomes larger with increasing photoelectron escape energy fluxes, especially above 500 km.

The discrepancies of these effects in the dusk and dawn sectors can be explained by the plasma drift along magnetic field lines, induced by the combined effects of ambi-polar diffusion and neutral-wind drag. In the dusk sector, the neutral-wind is directed to the north, while in the dawn sector the neutral wind points in the opposite direction. So, the escaping thermal plasma flow in the dusk sector is lower than in the dawn sector for nearly equal electron temperatures. It may be noted that the influence of electron heating fluxes from the plasmasphere on the electron density profiles of the upper ionosphere are small in the dusk sector but have a pronounced effect above 400 km in the dawn sector.
The model results for $N_e$ and $T_e$ profiles above EISCAT, as discussed up to this point, are obviously not unambiguously determined by the model input data set for the period under study. In order to obtain more precise information about the temporal-spatial distribution of the ionospheric parameters and to decrease the input data uncertainties involved in the modelling, we have used experimental data from the Active mission for the same time-periods.

A comparison of the $N_e$ measurements along the orbital track of the subsatellite Magion-2 with the model results is shown in Fig. 10. As already stated, the effects of convection and electron heating fluxes from the plasmasphere for this time-interval are unimportant at mid-latitudes and they will not be presented here. But the vibrationaly excited N$_2^*$ has an appreciable influence on $N_e$ and $T_e$ for all latitudes. The photoelectron escape energy fluxes at mid-latitudes were assumed with $2 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ in this case. As can be seen in Fig. 10, the model tends to overestimate the $N_e$ concentration along orbit 3812, when N$_2^*$ was not taken into account, and it has a reasonable agreement for the case with $T_e = 1.25 T_n$. Thus, if we accept that during quiet geomagnetic conditions the spatial distribution of $N_e$ concentration has no sudden latitude-longitude changes, we may assume that $T_e = 1.25 T_n$ is a reasonable value for all latitudes, including the EISCAT location. The assumption is quite reasonable, especially for our conditions of high solar activity in summer when the main ionospheric trough is absent.

Comparisons with atomic-ion concentrations along the Active orbital track with model results for orbit 3805 near 0325 UT are shown in Figs. 5–7. A good agreement between model and experimental data can be noticed for the case of ignored N$_2^*$ (Fig. 5). In the case with $T_e = 1.25 T_n$, the O$^+$ and H$^+$ concentrations are decreased. This effect is more prominent for the H$^+$ density at the latitudinal range from 60° to 70°. A further increase in $T_e$ causes a larger decrease in the atomic-ion concentrations in the high-latitude range.

The effects of different convection patterns on the atomic-ion density along orbit 3805 and the comparison with experimental data are shown in Fig. 6. It can be seen that a reasonable agreement between model results and orbital data at high latitudes are achieved for the cases with maximum FACs in the 10–22 MLT and 06–18–MLT meridional planes. It should be noted that a reasonable agreement was obtained between $N_e$ profiles over EISCAT and also model results for the same convection (Fig. 3).

Finally, the effects of different photoelectron escape energy fluxes on the O$^+$ and H$^+$ model concentrations along the orbit 3805 are also small, as can be seen in Fig. 7. But they show marked plasma-density depletions and $T_e$ increases near the EISCAT station where the fluxes were enhanced artificially. This is an effect of the thermal plasma outflow which is close to the regime of the polar wind above 1000 km. The upward proton flux depletes the H$^+$ density while affecting the O$^+$ density profile through its scale height. The latter process increases the O$^+$ scale height to the plasma scale height, which is larger than the individual O$^+$ scale height. Thus, the decrease of the O$^+$ concentration at 400–500 km altitude does not lead to an appreciable depletion of the O$^+$ density at 2000-km altitude. A more detailed explanation of this effect can be found, for example, in the paper of Blelly et al. (1992).

Thus, as indicated in Figs. 5–6, the case without vibrationally excited N$_2^*$ and a convection with maximum FACs reached in the 06–18–MLT plane is more preferable with regard to the experimental data of orbit 3805. But we should keep in mind that the model runs with $T_e = 1.25 T_n$ and the same convection pattern also give a reasonable agreement between model and orbital data.

### 7 Summary and conclusions

In this work we have made an effort to take advantage of the global thermosphere-ionosphere-plasmasphere model (GSM TIP) for the interpretation of the experimental data sets obtained for the same time-spans but separated in space. At the same time the study provided reliable inputs to the model by a reasonable matching of numerical model results with the experimental data sets obtained from three different sources: two orbits of the Active mission and CP-1 observations from the EISCAT station on day 212 (31 July) of 1990.

The satellite pair passed near the EISCAT station around 0325 and 1540 UT at an altitude of about 2000 and 2200 km, respectively, and the satellite data ($N_e$, $T_e$ and ion composition) were obtained onboard the Active main satellite and its subsatellite Magion-2. The period under study is generally characterized by high solar activity near the maximum of the 22nd solar cycle with an average value of $F_{10.7}$ of the solar radiation around 200.

The numerical model calculations were performed by using the MSIS-86 neutral-atmosphere parameters and with consideration of vibrationally excited nitrogen molecules.

Since one cannot derive all model inputs directly from experimental data for the period under study, we studied the influence of three main input parameters: the temperature of the vibrationally excited N$_2^*$, the convection electric-field patterns resulting from different FAC distributions and the photoelectron escape energy flux. They were adjusted to the observed values to provide a best fit. We obtained similarities between model behaviour on one side and satellite and EISCAT data on the other.

The detailed comparisons between the experimental data and the numerical model results have shown that the most preferable case can be obtained with the following model inputs set: the inclusion of N$_2^*$ with $T_e = 1.25 T_n$, maximum FACs reached at the 06–18–MLT meridional plane and a photoelectron escape energy flux of $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ over EISCAT and $2 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ for all other latitudes.

For these inputs, the electron density profiles above EISCAT are in qualitative agreement with the model results both at 0325 and 1540 UT, but the model $N_e$ concentration is a little lower (about 15 to 20 per cent) than
the EISCAT data. The comparison of the electron-temperature measurements with the model calculations at 0325 and 1540 UT for the same case has shown, in general, a good agreement as well, although the model tends to underestimate the $T_e$ values for both time-spans by about 100–200 K. The good agreement between the model meridional neutral-wind component and the corresponding values of the HWM93 empirical wind model for the EISCAT location supports the conclusions drawn.

The comparison of the model $N_e$ density along the Magion-2 orbital track 3812 with measured values has shown that the case with $T_e \sim 1.25 T_a$ is a good choice, providing a reasonable agreement between model and satellite data at all latitudes and confirming the result obtained for the EISCAT station at 1540 UT.

The measurements of O$^+$ and H$^+$ concentrations obtained in the dawn sector (0325 UT) by the Active main satellite show by comparison with the model results that the assumed convection pattern with maximum FACs in the 06–18 MLT meridional plane and the selected photo-electron escape energy flux of $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ are good input data, but an even better agreement was obtained if vibrationally excited N$_2^+$ was not taken into account for this case. The inclusion of N$_2^+$ in the model calculations with $T_e \sim 1.25 T_a$ causes a decrease in the O$^+$ and H$^+$ density in the high-latitude region by a factor of nearly two for H$^+$ and 20% for O$^+$, which is the main component at this altitude.

It should be noted here that all these discrepancies between model results and experimental data are related to various uncertainties involved in the modelling of the ionospheric situation under study and may be eliminated by some slight variation of the input data.

The sensitivity of the model results to the variation of three main input data has been studied in this work in detail. We found that the inclusion of vibrationally excited N$_2^+$ is very important for the period under study. The $N_e$ density at F2-region altitudes changes by a factor of 2 or more if one includes N$_2^+$, while the sensitivity of the density profile with respect to changed convection and electron heating flux variations from the plasmasphere is less pronounced and shows different behaviour at the dawn and dusk sectors.

Thus we conclude that the normal ionospheric convection pattern corresponding to quiet geomagnetic conditions obtained with maximum FACs reached in the 06–18 MLT plane are correct for these time-spans in the dawn and dusk sector. The inclusion of vibrationally excited N$_2^+$ in the model calculations is very important and the values of the excited N$_2^+$ temperature are near $T_e \sim 1.25 T_a$.

With respect to mid-latitudes, an enhanced photo-electron escape energy flux is required above the EISCAT station. Their values were assumed to be $2 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$ and $6 \times 10^{10}$ eV cm$^{-2}$ s$^{-1}$, respectively. It is possible that there is another significant source of heat for electrons of the upper ionosphere and plasmasphere, but the limited experimental data base makes it difficult to determine unequivocally what is physically taking place.

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Appendix A: heating by photoelectrons

Heating rates of the electron gas are calculated using the following analytic formulas.

\[ Q_e(s) = Q_{el}(s) + Q_{nl}(s), \]  

\[ Q_{el}(s) = \varepsilon q_e(s), \]  

\[ Q_{nl}(s) = Q_{nl}(s), \]

where \( Q_{el} \) is the local heating rate and \( Q_{nl} \) the non-local heating rate. The local heating rate is calculated by the well-known formula

\[ Q_{el}(s) = \varepsilon q_e(s), \]

where \( \varepsilon \) is efficiency of the local heating electron gas, and \( q_e(s) \) is the photoionization rate. The efficiency has been taken according to Krinberg (1978) in the following form

\[ \varepsilon = 0.16\left[9 + \ln(N_e(s)/N_e(s))^2\right][eV]. \]

Here \( N_e(s) \) is the electron concentration and \( N_e \) is the sum of neutral-particle concentration. The non-local heating rate is approximated by the following analytic formula according to Matafonov (1986)

\[ Q_{nl}(s) = Q(s) \frac{B(s)}{B_0(s)} \frac{N_e(s)}{N_e(s)} ds, \]

with

\[ Q(s) = q_s(s) \left(1 + \left(1 + \frac{E_s}{E_a}\right) \exp \left(-\frac{E_s}{E_a}\right) \right), \]

\[ E_a = 1.3(\ln N_e - 11)^2 + 1.2, \]

\[ N_e = \frac{1}{s} \frac{B_s(s)}{B(s)} N_s(s) ds. \]

In these expressions \( B_s \) is the magnetic field intensity at the lower boundary, i.e. at the ionospheric foot points of the geomagnetic field lines at an altitude of 175 km; the variable \( s \) refers to pathlength along \( B_s \); \( L \) and \( S \) correspond to the northern and southern boundaries of the field lines; \( E_a \) is the average energy of the photon-electrons (set to 10 eV for this study); \( N_e \) is the total electron content and \( q_s \) is maximal escape energy flux of suprathermal electrons into the plasmasphere (set to \( 2 \times 10^{-8} \text{eV cm}^{-2} \text{s}^{-1} \)).

Appendix B: vibrationally excited nitrogen

Effects of vibrationally excited molecular nitrogen (N²⁺) on the electron concentration are carried out by means of the loss-rate variation for O⁺ ions in the reaction

\[ \text{O}^+ + \text{N}^2_2 \rightarrow \text{NO}^+ + \text{N}. \]

\[ \]  

The rate coefficient \( \beta_i \) for this reaction without taking into account \( N^2_2 \) is given by the well-known formula of St.-Maurice and Torr (1978). A correction of this rate coefficient for \( N^2_2 \) is made in correspondence with the works of Pavlov (1986, 1988) in the following way. Let us consider the effective rate coefficient \( \beta^* \) as

\[ \beta^* = \sum_{i=0}^{\infty} \beta_i N_i, \]

where \( \beta_i \) are the rate coefficients of reaction B1 for the \( i \)th excited level of \( N_2 \) with a number density \( N_i \); \( \beta^* \) is the rate coefficient without consideration of \( N^2_2 \). The coefficients \( \beta_i \) for the first, second and third vibrational levels can be written as

\[ \beta_i = A_i T_n + B_i, \]

where

\[ A_i = 3.391 \times 10^{-15} \quad 2.234 \times 10^{-14} \quad 3.022 \times 10^{-14} \text{K}^{-1} \text{ cm}^3 \text{ s}^{-1}, \]

\[ B_i = 3.722 \times 10^{-13} \quad 3.085 \times 10^{-11} \quad 1.921 \times 10^{-10} \text{cm}^3 \text{ s}^{-1}. \]

\[ T_n \] is the temperature of the neutral gas. For a Boltzmann distribution we get

\[ N_i = \sum N_i = (1 - \exp(-3353/T_n)) \exp(-3353/T_n), \]

where \( T_n \) is the temperature of \( N^2_2 \). The main cooling rate of the electron gas by \( N^2_2 \) was calculated using the formula of Stubbe and Varnum (1972).