Modularity, Lead time and Return Policy for Supply Chain in Mass Customization System

Jizi Li*
CSC Networks System Research Centre, Wuhan Textile University, Wuhan, Hubei Province, 430073, RP China
E-mail: lijison.csc@qq.com

Chunling Liu
CSC Networks System Research Centre, Wuhan Textile University, Wuhan, Hubei Province, 430073, RP China
E-mail: liuchunring@gmail.com

Weichun Xiao
CSC Networks System Research Centre, Wuhan Textile University, Wuhan, Hubei Province, 430073, RP China
E-mail: 835452199@qq.com

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Abstract
Mass Customization (MC) is a flexible manufacturing system with features of Mass Production (MP) and Customization Production (CP). However, there is few researches about competition & cooperation between the upstream MP firm (module manufacturer) and downstream CP firm (assembler) under MC supply chain scenario. From supply chain perspective, this paper first develops the base models considering the influences of return policy, modularity level, production lead time and pricing factors. Furthermore, according to the different decision-making situations, three kinds of MC supply chain models in competitive or cooperative environment (i.e. simultaneous-move game, sequential-move game and the cooperative game) have been built, then, the optimal solution of each model have been analyzed and compared, and coordination mechanism is design to cooperate in MC supply chain via profit-sharing with Nash bargaining power. Finally, through the numerical analysis, we find the highest profit is from the cooperative setting, then followed by in simultaneous-move and sequential-move one, the reason is that the lowest product price and the largest market demand easily occurs in the cooperative game compared with the others, the upstream module manufacturer takes advantage of MP to increase the modularity level and decrease manufacturing cost for the whole supply chain, the downstream assembler task is to shorten the lead time according to customer’s needs, while the wholesale price in cooperative game higher than simultaneous-move game and sequential-move game can ensure each firm’s benefits, effectively prevent from the effect of double marginalization and obtain Pareto optimality.

Keywords: Mass customization; supply chain; return policy; modularity; lead time

* Corresponding author: lijison.csc@qq.com, Tel: +(86)027 5936 3271
1. Introduction

In recent years, consumers are increasingly demanding products that closely match their individual preferences, meanwhile advances in manufacturing and information technologies make it possible to efficiently integrate both MP (Mass Production) and CP (Customization Production) in a new operational context for satisfying this demand [1][2]. This approach responding to tailored demand is generally called as Mass Customization (MC), whereby firms use a make-to-order process that gives consumers exactly what they ask for. MC relates to the ability to provide customized products or services through flexible processes in high volumes and reasonably low costs [3][4]. Many authors propose similar but narrower, more practical concepts. They define MC as a system that uses information technology, flexible processes, and organizational structures to deliver a wide range of products and services that meet specific needs of individual customers, at a cost similar to MP. In any case, MC is seen as a systematic idea involving all aspects of development, production, product sale, and delivery, full-circle from the customer option up to receiving the finished product. MC has been widely implemented in industries such as consumer electronics and is currently popular in the fashion industry [5][6][7]. For example, sportswear brands such as Adidas, Nike and Puma, as well as luxury fashion brands such as Coach, Christian Dior, Gucci, Cartier and Hermes, are all implementing MC. The justification for the development of MC systems is based on three main ideas. First, there is an increasing demand for product variety and customization. Secondly, new flexible manufacturing and information technologies enable production systems to deliver wider variety at lower cost. Finally, the shortening of product life cycles and expanding industrial competition has led to the breakdown of many mass industries, increasing the need for production strategies focused on individual customer.

Nowadays, many current MC programs are developed online and supported by the internet technologies. Therefore, customers may only specify what they want via an online platform without really seeing and touching the real product before the product is assembled and delivered [8][9][10][11][12]. For many customers, the final customized products may fail to meet their expectation, resulting in their desire to return the MC products for a partial or full refund. However, on one hand, most MC companies, such as JC Penney and Ralph Lauren, hesitate to accept product return unless the product is proven to be defective in customized-production or delivery [8]. On the other hand, it is thus impossible for a firm to gain competitive advantage if it does not offer a return policy for products under MC setting [13][14]. Studies have shown that customers perceive the option of return as one of the main factors affecting the buying decision and that the majority of customers are likely to pay attention to the return policy before deciding to shop [15].

It is noted that a generous return policy would increase the probability of return and also increase the cost of doing business, due to uselessness or limited reuse of returns of customized product[13][14][15]. So in formulating a return policy for MC products, the firm faces a trade-off between offering a generous return policy and suffering the costs resulting from the returns. These disadvantages from return policy could be offset by product modularity which for the first time was proposed by Mukhopadhyay and Setoputro [14]. For example, when a modular product containing a number of standard parts is returned, it can be very easily dismantled and reassembled without damaging their values. It is clear that the higher the degree of product modularity, the lower is the loss [16][17]. In other words, the company will incur a lower cost for handling return product when the level of modularity is higher. Therefore, to some extent, determining the level of modularity and return rate is key issue for supply chain implementing MC. In order to solve this problem, the analysis of MC operation requires to take into account the entire supply chain system including upstream’s modular design and production, downstream assemble, sales and return.

In the process of modularity design, it needs classifying modularity components into two distinct categories: standard commonality and customized parts [18][19]. In this way, standard commonality and customized parts could be filtered out and effectively and efficiently manufactured under MC system in supply chain context. In details, the standard commonality in large volume can be mass-produced by the upstream firm, which achieves economics of scale and production quality guarantees, while the customized
parts can be customized-produced and assembled by the downstream firm on basis of the consumer special requirement, hence it ensures that the consumers’ specification and shorter response time can be satisfied [20][21]. In the MC setting, the point that departs the supply chain into two stages--upstream MP mode and downstream CP mode, is called customer order decoupling point (CODP) (seen in Fig.1). The closer the CODP gets to the upstream firm, the higher the degree of customized-production and the lower of the degree of standardization, and vice versa [22]. Thus, in the supply chain context, it means that the goal for upstream firm is to reduce the production cost, while the goal for downstream firm is to satisfy the consumers’ requirements (such as product function, lead time) [23].

For the researches of MC, a majority of literatures mainly focus on the MC implementation as a whole, few researches pay more attention to that how to coordinate in different functional firms (i.e. upstream MP firm and downstream CP firm) along MC supply chain. For instance, Yang & Kincade & Chen proposed structured categories of apparel MC in a matrix based on modularity and variety levels for the attributes of design and fit, and provided examples of the implementation of MC using the matrix [24]. Zhang & Zhao & Qi examined the effects of organizational flatness, coordination and product modularity on mass customization capability (MCC) development, and found that product modularity, cross-functional coordination and supply chain coordination significantly contribute to MCC, whereas the influences of cross-plant coordination and organizational flatness are insignificant [25]. In addition, Mavridou & Kejangias & Tzovaras & Hassapis introduced a mass customization recommender system, this system exploited data mining techniques on automotive industry customer data aiming at revealing associations between user affective needs and the design parameters of automotive products [26]. Shao integrated product strategy and channel design to explore whether the firm should adopt mass customization and how the distribution channel should be configured for custom products [27].

Theoretically, the intention for all of supply chain members is to improve the end customer satisfaction. In fact, upstream mass-produced firm and downstream customized-produced and assembled firm belong to two different entities, it is well documented that the asymmetric information will drive the members to maximize their own profits, which influence the MC operation performance. For example, In China, this kind of phenomenon occurs in many industries such as injection machine and metal fittings industry in Ningbo and Wenzou City of Zhejiang Province. On one hand, the majority of firms become more and more specialized, and focus on the smaller part of supply chain, some of them are mass-production style. On the other hand, downstream customized-produced firms have to tailor and detail final products and sell them via the Internet, both upstream and downstream sides exist game relationship. Though some literatures [28][29] have studied the competition (game) model between upstream and downstream firms along supply chain, such as Alptekinoglu & Corbett studied competition between two multi-product firms with distinct production technologies (MP and MC), and analyzed the subgame-perfect Nash equilibrium in the three-stage game, i.e., the firms simultaneously decide whether to enter the market, next, the MP and MC choice, finally, both firms simultaneously set prices [30]. Xia & Rajagopalan used the duopoly game model to determine the choice of MP and MC modes in different firms [31]. Xie & Wei investigated the game problems by seeking optimal cooperative advertising strategies and equilibrium pricing in a two-member distribution channel [32]. Mendelson & Parlakturk analyzed the optimal product lines of firms that sell standard or individually customized products and solved the resulting equilibrium for both monopoly and duopoly of traditional and customizing firms [33]. However, there is few researches of game-theoretic models addressing both the upstream MP firm and downstream CP firm under MC supply chain scenario. So, in this paper, we will explore how different functional firms (i.e. upstream MP firm and downstream CP firm) compete and cooperate along supply chain and perfectly integrate together to reach the MC goal.

Therefore, the main contributions of this paper are as follows: (1) We convert the two parties of (manufacturer and the customer) supply chain model of Konstantaras et al. [13] into the other two parties of MC supply chain (upstream MP firm, downstream CP assembler). (2) We consider the lead time of the downstream CP firm as a decision variable, which has been rarely considered in the previous literatures. (3) We analyze how the game between upstream MP firm and downstream CP assembler influence the optimal decisions and consider...
three models (simultaneous move game, sequential move game and cooperative game) where consumer demand is determined by retail price, refund rate and lead time. After comparing cooperative strategy with competitive (simultaneous move game and sequential move game) ones, discusses how a cooperative solution could be sustained over time.

The rest of this paper is configured as follows: the assumptions and the base problem formulation are presented in Section 2. In Section 3, we develop three extended models including two competitive game models (i.e. simultaneous-move and sequential-move) and one cooperative one. Then, the coordination mechanism is designed in section 4. In section 5, the numerical studies and sensitive analysis are provided. Finally, we draw a brief of conclusions and provide future research directions in Section 6.

2. Assumption and base model formulation

2.1. Assumption

We consider an MC supply chain system consisting of three parties, namely a customer placing an order, an assembler which assembles and sells customized products to the customer and a module manufacturer which produces and wholesales modules to the assembler in MP way. The product is modular in structure. The sequence of action under MC program is stated as follows. A customer orders a product to a certain specification; The assembler purchases standard modules from the module manufacturer and builds up the product, then sells it at a price \( p \); The manufacturer produces modules and determines the level of modularity \( m \), where \( 0 \leq m \leq 1 \), as well as the wholesale price \( w \). In the literatures related to customized products, the price is generally treated as a fixed exogenous parameter. In this paper, the customized product price is treated as a decision variable. In case, if the product does not meet the customer’s expectations, the assembler allows return, and the customer will receive a partial or full refund of \( r \), where \( 0 \leq r \leq p \). When a customized product which is assembled by modules is returned, it is easily disassembled into a number of modules and built into new customized products. The degree of reuse of the return product is critically related to the level of modularity, a higher \( m \) means a higher degree of reuse for the assembler but higher cost for the manufacturer. At the same time, determining the value for \( r \) is not an easy task as many aspects of the problem have to be considered. So the refund value is treated as another decision variable for the assembler. Moreover, the lead time \( t \) should be taken into consideration under MC supply chain scenario, which is negatively related to the level of modularity and will influence the market demand [31][34].

\[
D = D_b + E \cdot p + J \cdot r + G \cdot t
\]

Where \( D_b \), \( E \), \( J \), and \( G \) are all \( > 0 \). \( D_b \) is the base demand, which depends on factors such as product quality, brand image, and general economic factors; \( E \) is price-demand sensitivity coefficient; \( J \) is refund-demand sensitivity coefficient; \( G \) is lead-time-demand sensitivity coefficient. For the module manufacturer, the demand of module units is equal to the demand of customized products.

The assembler allows the customer to return the customized product for a refund of \( r \). While this will improve the customer satisfaction and also generate more returned products from the customer. Similar to \( D_r \), the number of returns can be denoted as \( R_{(r)} = \phi + \psi r \). Where \( R_{(r)} \) is returned quantity, \( \phi \) is base return quantity independent of the refund \( r \), \( \psi \) is parameter of return quantity [13].

As refer to cost of the downstream assembler, we use two types of costs. First, denoted by \( F_d \) is the
fixed cost including investment in assembly line. However, comparing to huge demand in mass products, the needed quantity of customized products is very small, so the variable cost of customized product is not considered in this paper [38], thus, the second cost, denoted by \( C_{(r,m)} \), is the value lost per unit of the product that has been returned by the customer, is modeled by the function: \( C_{(r,m)} = r - \nu m \), where \( \nu \) is the unit reusability value of the returned product, \( 0 \leq \nu \leq \frac{r}{m} \). Obviously, if the modules used in the product is highly modularized, the lost will be low. Similarly, for the upstream manufacturer in mass production, we also use two types of costs. The fixed cost \( F_M \) associated with efforts to increase the modularity level \( m \), such as high investment, as it requires, designing skills, research and technology, which is assumed as: \( F_M = \frac{1}{2} \kappa m^2 + \eta \), is increasing and convex in \( m \), and the variable cost \( C_{M(m)} = \varepsilon m \). Where \( \kappa, \eta, \varepsilon \) are positive parameters, \( \kappa, \eta >> 0 \) [39][40].

In order to simplify the model, without lose of generality, we assume that the assembler’s lead time \( t \) is a negative linear function of \( m \), while the wholesale price \( w \) is a positive linear function of \( m \), which is similar to the model considered by Na Liu et al. [8]. That is, \( t = x - ym \) and \( w = \theta + \varepsilon m \), where \( x, y, \theta \) are positive parameters [41][42].

### 2.2. Model formulation

With the above analysis, the customized assembler’s and module manufacturer’s profit functions can be expressed as follows:

\[
\pi_A = D_{(p,r,t)}(p-w) - R_{(r)}C_{(r,m)} - F_A \tag{1}
\]

\[
\pi_M = D_{(p,r,t)}(w-C_{M(m)}) - F_M \tag{2}
\]

Subject to: \( 0 \leq r \leq p \); \( 0 \leq m \leq 1 \)

By re-organizing the profit functions, Eqs. (1) and (2) can be rewritten as:

\[
\pi_A = (\alpha - \beta p + \nu r - \delta(x - ym))(p - \theta - \varepsilon m) + (\phi + \nu r - \delta(x - ym)) - (x - ym) \theta - \frac{1}{2} \kappa m^2 + \eta \tag{3}
\]

\[
\pi_M = \left[ \alpha - \beta p + \gamma r - \delta(x - ym) \right] \theta - \frac{1}{2} \kappa m^2 + \eta \tag{4}
\]

**Theorem 2.1** Under the condition of \( 4\beta \nu r - \gamma^2 > 0 \), the assembler’s profit function is concave in \( p, r \), and has unique maximum solution.

**Proof.** The Hessian matrix of the assembler’s profit is

\[
H_{\pi_A} = \begin{pmatrix}
\frac{\partial^2 \pi_A}{\partial p^2} & \frac{\partial^2 \pi_A}{\partial p \partial r} & \frac{\partial^2 \pi_A}{\partial r^2}
\end{pmatrix} = \begin{pmatrix}
-2\beta & \gamma \\
\gamma & -2\nu
\end{pmatrix}
\]

\[|-2\beta| < 0; \quad \begin{vmatrix} -2\beta & \gamma \\ \gamma & -2\nu \end{vmatrix} = 4\beta \nu r - \gamma^2 > 0\]

From the above, \( H_{\pi_A} \) is a negative definite matrix provided that \( 4\beta \nu r - \gamma^2 > 0 \). Thus, the assembler’s profit function is concave in \( p, r \), and has unique maximum solution. □

It is noted that \( \beta \) is price-demand sensitivity coefficient, \( \gamma \) is refund-demand sensitivity coefficient. Obviously, \( 4\beta \nu r - \gamma^2 > 0 \) will hold provided that the market demand is more largely influenced by price-demand coefficient than other coefficient. Actually, it is true in real world of MC market. Thus, the assembler can get the maximum profit by taking the first order derivative of \( \pi_A \) respect to \( p \) and \( r \).

**Theorem 2.2** Under the condition of \( -\kappa < 0 \), the manufacturer’s profit function is concave in \( m \), and has unique maximum solution.

**Proof.** The second order derivative of \( \pi_M \) respect to \( m \) is \( \frac{\partial^2 \pi_M}{\partial m^2} = -\kappa \). Obviously, the manufacturer’s profit function is concave in \( m \) if and only if \( -\kappa < 0 \) holds. □

For the module manufacturer, the fixed cost coefficient \( \kappa \) is a large constant, obviously, \( -\kappa < 0 \) will hold. Thus, the manufacturer can obtain the maximum profit by taking the first order derivative of \( \pi_M \) respect to \( m \).

### 3. Decision-making models

#### 3.1. Decision-making in competitive environment

There are two possible situations in the competitive environment: simultaneous and sequential moves [43].

**3.1.1 Simultaneous moves**

The supply chain members determine their own
decision variables independently due to the asymmetric information. When the downstream assembler and the upstream module manufacturer have the same decision power in MC context, they simultaneously maximize their own profits. This situation is called a simultaneous-move game and the solution provided by this structure is called the Nash equilibrium.

Specifically, the decision problem is:

\[
\begin{align*}
\max_{p,r} & \quad \pi_A^N = D(p,r) - R_c C_{A(m)} - F_A \\
\max_{m} & \quad \pi_M^N = D(p,r) - C_{M(m)} - F_M \\
\text{s.t.} & \quad 0 \leq r \leq p \\
\text{s.t.} & \quad 0 \leq m \leq 1
\end{align*}
\]

According to Theorem 2.1 and Theorem 2.2, the first order conditions for extreme points of \(\pi_A^N\) and \(\pi_M^N\) are:

\[
\frac{\partial \pi_A^N}{\partial p} = 0; \quad \frac{\partial \pi_A^N}{\partial r} = 0; \quad \frac{\partial \pi_M^N}{\partial m} = 0
\]

Solving Eq. (6), the unique optimal decisions of this system are:

\[
p_A^{N*} = \frac{2\alpha \psi - \gamma^2 \theta - \gamma \phi - 2x\delta \psi + 2\beta \theta \psi}{4\beta \psi - \gamma^2} + \frac{y \delta \theta (\psi \gamma \psi + 2y \delta \psi + 2\beta \psi \psi - \gamma^2 \epsilon)}{\kappa (4\beta \psi - \gamma^2)}
\]

\[
r_A^{N*} = \frac{\alpha \gamma - x \gamma \delta - \beta \gamma \theta - 2\beta \phi}{4\beta \psi - \gamma^2} + \frac{y \delta \theta (\psi \gamma \psi + 2y \delta \psi + 2\beta \psi \psi - \gamma^2 \epsilon)}{\kappa (4\beta \psi - \gamma^2)}
\]

\[
m_M^{N*} = \frac{\delta \gamma \theta}{\kappa}
\]

\[
w_M^{N*} = \frac{\gamma \delta \theta}{\kappa}
\]

From the above optimal decisions, we have the following important observations.

**Proposition 3.1** If the price-demand sensitivity coefficient \(\beta\) increases: \(p_A^{N*}\) will decrease, \(r_A^{N*}\) will decrease provided that \(y \delta \theta (2\psi \psi - 2\epsilon) \leq \kappa (\gamma \theta + 2\phi)\).

**Proof.** \(p_A^{N*}\) can be rearranged as

\[
p_A^{N*} = \frac{2\alpha \psi - \gamma^2 \theta - \gamma \phi - 2x\delta \psi}{4\beta \psi - \gamma^2} + \frac{y \delta \theta (\psi \gamma \psi + 2y \delta \psi + 2\beta \psi \psi - \gamma^2 \epsilon)}{\kappa (4\beta \psi - \gamma^2)} + \frac{2\theta \psi \beta + 2y \delta \theta \psi \beta}{\kappa (4\beta \psi - \gamma^2)}
\]

when \(\beta\) increases, \(2\alpha \psi - \gamma^2 \theta - \gamma \phi - 2x\delta \psi \) will decrease.

\[
\frac{2\theta \psi \beta + 2y \delta \theta \psi \beta}{\kappa (4\beta \psi - \gamma^2)}
\]

\[
\frac{y \delta \theta (\psi \gamma \psi + 2y \delta \psi + 2\beta \psi \psi - \gamma^2 \epsilon)}{\kappa (4\beta \psi - \gamma^2)}
\]

\[
\frac{2\theta \psi \beta + 2y \delta \theta \psi \beta}{\kappa (4\beta \psi - \gamma^2)}
\]

while \(\beta\) increases, \(2\alpha \psi - \gamma^2 \theta - \gamma \phi - 2x\delta \psi \) will decrease.

It is relatively intuitive. When price-demand sensitivity coefficient \(\beta\) increases, increasing retail price \(p_A^{N*}\) implies a more significant decrease in the market demand. It would be better for the assembler to decrease the refund rate to improve performance when the price-demand sensitivity coefficient is larger than the refund-demand sensitivity one, provided that \(\kappa\) is a large constant which is mild and can be satisfied in most cases.

**Proposition 3.2** If refund-demand sensitivity coefficient \(\gamma\) increases: \(r_A^{N*}\), \(p_A^{N*}\) will increase provided that \(\kappa (\alpha - x \delta - \beta \theta) + y \delta \theta (y \delta - \beta \epsilon) > 0\).
Proof. Rearranging $r_{A}^{N^{*}}$, we have
\[
r_{A}^{N^{*}} = \frac{\kappa(\alpha - x\delta - \beta\theta + y\delta(\gamma\delta - \beta\varepsilon))\gamma}{\kappa(4\beta\psi - \gamma^{2})} - \frac{2\beta\phi\kappa - 2\beta\psi y\delta\theta}{\kappa(4\beta\psi - \gamma^{2})}
\]
When $\gamma$ increases, the denominator of $r_{A}^{N^{*}}$ decreases, thus, $r_{A}^{N^{*}}$ will increase provided that $\kappa(\alpha - x\delta - \beta\theta + y\delta(\gamma\delta - \beta\varepsilon)) \geq 0$, which will hold if $\alpha\kappa$ is a large enough constant. □

When refund-demand sensitivity coefficient $J$ increases, in order to attract consumers, the assembler will offer a more generous refund provided that $0 \leq y \leq \gamma$, which is mild and can be satisfied in most cases. However, in order to compensate the profit, the assembler has to increase the retail price. By Embedding $p_{A}^{N^{*}}$, $r_{A}^{N^{*}}$, $t_{A}^{N^{*}}$, $m_{M}^{N^{*}}$ and $w_{M}^{N^{*}}$ into $D_{(p,r)}$, $\pi_{A}^{N}$ and $\pi_{M}^{N}$, the market demand and maximum profit can be rewritten as:
\[
D_{(p,r)} = \frac{2\beta\psi(\gamma^{2}\delta\theta - y\beta\delta\varepsilon\theta + (\alpha - x\delta - \beta\theta)\kappa)}{\kappa(4\beta\psi - \gamma^{2})} + \frac{\gamma\beta(y\delta\psi\kappa - \eta\phi)}{\kappa(4\beta\psi - \gamma^{2})}
\]
\[
\pi_{A}^{N} = \left[\alpha - \beta p_{A}^{N^{*}} + \gamma r_{A}^{N^{*}} - \delta(x - ym_{M}^{N^{*}})\right]\left[p_{A}^{N^{*}} - \theta - \varepsilon m_{M}^{N^{*}}\right] - (\phi + \psi r_{A}^{N^{*}})\left(r - v m_{M}^{N^{*}}\right) - F_{A}
\]
\[
\pi_{M}^{N} = \left[\alpha - \beta p_{A}^{N^{*}} + \gamma r_{A}^{N^{*}} - \delta(x - ym_{M}^{N^{*}})\right]\theta - \left(\frac{1}{2}\kappa m_{M}^{N^{*}2} + \eta\right)
\]
\[
\pi_{w}^{N} = \left[\alpha - \beta p_{A}^{N^{*}} + \gamma r_{A}^{N^{*}} - \delta(x - ym_{M}^{N^{*}})\right]\left[p_{A}^{N^{*}} - \theta - \varepsilon m_{M}^{N^{*}}\right] - (\phi + \psi r_{A}^{N^{*}})\left(r - v m_{M}^{N^{*}}\right) - \left(\frac{1}{2}\kappa m_{M}^{N^{*}2} + \eta\right) - F_{i}
\]

3.1.2 Sequential moves

Under asymmetric information and competitive environment, the order of sequential moves may reveal private information. Considering that assembler’s role is to assemble components from module manufacturer, while that module manufacturer’s functions are to produce or make modules. On this MC supply chain scenario, the assembler is middle-located in supply chain. The advantages of assembler usually come from information accumulation from upstream and downstream firms. In other words, assembler first collects demand from downstream consumer, then asks upstream module manufacturer whether they have capability of making the relevant modules, finally assembles the finished products. It means that the middle-located companies largely depend on technology and modularity of upstream supplier. Meanwhile, they are driven by the downstream consumer. Based on this, the assembler could not dominate in MC supply chain. For instance, In China in smart phone industries, such as Mi, ViVo companies belong this category. Thus, the assembler infers information by observing the module manufacturer’s actions. The sequencing of moves becomes subtler, as it reflects each firm’s calculated tradeoff between the early mover advantage and the informational benefit of waiting to learn rival’s private information (i.e. information revelation).

We now model the relationship between the module manufacturer and the assembler as a sequential non-cooperative game with the module manufacturer as the leader and the assembler as the follower. The solution of this leader-follower game is called the Stackelberg assembler equilibrium. In order to determine the Stackelberg equilibrium by backward induction, we first solve the assembler’s optimal problem when the module manufacturer’s decision variable $m_{M}^{N}$ and $w_{M}^{N}$ are given. Next, the optimal values of $m_{M}^{N}$ and $w_{M}^{N}$ are determined by maximizing the manufacturer’s profit function. Hence it gives rise to the following optimization problems.

\[
\begin{align*}
\text{Max}_{m,w} \pi_{M}^{N} &= D_{(p,r)}\left(w - C_{M(m)}\right) - F_{M} \\
\text{s.t.} \quad \text{Max} \pi_{M}^{N} &= D_{(p,r)}\left(p - w_{M}^{N}\right) \\
&\quad - R_{(r)}C_{d(r,m)} - F_{A} \\
\text{s.t.} \quad 0 \leq r \leq p \\
&\quad 0 \leq m \leq 1
\end{align*}
\]

Similarly to the simultaneous-move game case above, the assembler’s profit function $\pi_{A}^{N}$ is a concave function with respect to $p$, $r$. We can solve the two first order equations $\frac{\partial \pi_{A}^{N}}{\partial p} = 0$ and $\frac{\partial \pi_{A}^{N}}{\partial r} = 0$ to get the optimal decisions:
\[
p_A^s = \frac{\left(v\gamma\psi + 2\gamma\delta\psi + 2\beta\psi\rho - \gamma^2\phi\right)m_M^s}{4\beta\psi - \gamma^2} - \frac{\gamma^2\theta + \gamma\psi - 2\alpha\psi + 2\beta\psi\rho - 2\beta\theta\psi}{4\beta\psi - \gamma^2} \tag{17}
\]
\[
r_A^s = \frac{\left(v\gamma\delta - \beta\gamma\phi + 2\nu\beta\psi\rho\right)m_M^s}{4\beta\psi - \gamma^2} + \frac{\alpha\gamma - \chi\gamma\delta - \beta\gamma\theta - 2\beta\phi}{4\beta\psi - \gamma^2} \tag{18}
\]

Where \( p_A^s \) and \( r_A^s \) are determined by Eqs. (17) and (18) respectively.

The corresponding first-order condition with respect to \( m_M^s \) is \( \partial \pi_A^s / \partial m_M^s = 0 \). Thus, the optimal decision is:
\[
m_M^s = \frac{\theta\beta\left(v\gamma\psi + 2\gamma\delta\psi - 2\beta\psi\rho\right)}{\kappa\left(4\beta\psi - \gamma^2\right)} \tag{19}
\]
Eqs. (7), (17) and (18) lead to the Stackelberg equilibrium results:
\[
p_A^s = \frac{2\alpha\psi + 2\beta\theta\psi - \gamma^2\theta - \gamma\psi - 2\beta\psi\rho}{4\beta\psi - \gamma^2} + \frac{\beta\theta\psi\left(\nu\gamma\psi + 2\nu\beta\delta\psi - 2\beta\psi\phi\right)}{\kappa\left(4\beta\psi - \gamma^2\right)^2} \tag{20}
\]
\[
r_A^s = \frac{\alpha\gamma - \chi\gamma\delta - \beta\gamma\theta - 2\beta\phi}{4\beta\psi - \gamma^2} + \frac{\theta\left(\nu\gamma\psi - \beta\psi\phi + 2\nu\beta\psi\rho\right)\left(v\beta\gamma\psi + 2\nu\beta\delta\psi - 2\beta\psi\phi\right)}{\kappa\left(4\beta\psi - \gamma^2\right)^2} \tag{21}
\]
\[
m_M^s = \frac{\theta\beta\left(v\gamma\psi + 2\gamma\delta\psi - 2\beta\psi\rho\right)}{\kappa\left(4\beta\psi - \gamma^2\right)} \tag{22}
\]
\[
w_M^s = \frac{\theta\beta\left(v\gamma\psi + 2\gamma\delta\psi - 2\beta\psi\rho\right)\nu\psi}{\kappa\left(4\beta\psi - \gamma^2\right)^2} \tag{23}
\]

From the above optimal decisions, we have the following important observations.

**Proposition 3.3** If the refund-return-quantity coefficient \( \psi \) increases, \( p_A^s \) will decrease if \( \beta\theta \geq \chi\delta \); \( r_A^s \), \( m_M^s \) and \( w_M^s \) will decrease while \( r_A^s \) will increase if \( \nu\gamma + 2\gamma\delta - 2\beta\phi \geq 0 \).

**Proof.** With the same method in Proof of Proposition 3.1, when \( \psi \) increases, the right portion of \( p_A^s \) decreases, the left portion of \( p_A^s \) also decrease provided that \( 2\beta\theta\psi - 2\chi\delta\psi \geq 0 \), that is \( \beta\theta \geq \chi\delta \); thus, \( p_A^s \) will decrease. Similarly, the left portion of \( r_A^s \) will decrease, the right portion also decrease while \( v\beta\gamma\psi + 2\nu\beta\delta\psi - 2\beta\psi\phi \geq 0 \), that is \( v\gamma + 2\gamma\delta - 2\beta\phi \geq 0 \), consequently, \( r_A^s \) will decrease. In the same way, we know that \( m_M^s \) will decrease if \( v\gamma\psi + 2\gamma\delta\psi - 2\beta\psi\phi \geq 0 \), that is \( v\gamma + 2\gamma\delta - 2\beta\phi \geq 0 \). Due to the linear relationship to \( m_M^s \), the trends of \( w_M^s \) and \( r_A^s \) are obvious. \( \square \)

When the coefficient \( \psi \) increases, the consumer is more likely to return their products even though the products are customized. Thus, in order to cut down return quantity, the assembler has to reduce the refund rate, however, the market demand will also be shrunk. Thus, the only way for the assembler to increase the profit is to cut down the retail price provided that \( \beta\theta \geq \chi\delta \), that is the market demand is greatly influenced by the retail price. While for the module manufacturer, if \( \nu\gamma + 2\gamma\delta - 2\beta\phi \geq 0 \), that is, the unit reusability value of the returned product \( v \) is rather high, the demand of the new modules will decrease greatly for the reuse of the returned products, thus, the manufacturer will decrease his modularity level to compel the assembler to order new modules. Obviously, this is the main reason of inefficiency in the Non-cooperative supply chain.

By Embedding \( p_A^s, r_A^s, t_A^s, m_M^s \) and \( w_M^s \) into \( D_{(p,t)} \), \( \pi_A^s \) and \( \pi_M^s \), the market demand and maximum profit can be rewritten as:
\[
D^s = \frac{\left(2\alpha\psi - \gamma\phi - 2\chi\delta\psi - 2\beta\theta\psi\right)}{4\beta\psi - \gamma^2} + \frac{\beta\gamma\psi\phi^2\left(\nu\gamma + 2\gamma\delta - 2\beta\phi\right)}{\kappa\left(4\beta\psi - \gamma^2\right)^2} \tag{25}
\]
\[
\pi_A^s = \left[\alpha - \beta p_A^s + \gamma r_A^s - \delta\left(x - y m_M^s\right)\right] p_A^s - \epsilon m_M^s \tag{26}
\]
\[
\pi_M^s = \left[\alpha - \beta p_A^s + \gamma r_A^s - \delta\left(x - y m_M^s\right)\right] \theta - \left(1 - \frac{1}{2}\right) \kappa m_M^s \tag{27}
\]
3.2. Decision-making in cooperative environment

In the previous two subsections, we have analyzed two Non-cooperative game structures (a simultaneous move game and a sequential move game). However, if the supply chain members agree to cooperate, they negotiate to make joint decisions that eliminate supply chain inefficiency. In this section, we focus on a cooperative game structure in which both the module manufacturer and the customization assembler agree to make decisions that maximize the total MC supply chain profits.

The MC supply chain profits is described by $\pi^C = \pi^A + \pi^M$ and depends only on $p^C_A$, $r^C_A$, and $m^C_M$. We hence have the following optimization problem:

$$
\text{Max } \pi^C = D_{(p,r)}(p^C_A - \varepsilon m^C_M) - R_{(r)}C_{(r,m)} - \left(\frac{1}{2}\kappa m^C_M + \eta\right) - F_A
$$

subject to $0 \leq r \leq p$; $0 \leq m \leq 1$.

**Theorem 3.1** Under the condition of $4\beta\psi - \gamma^2 > 0$ and $(\gamma^2 - 4\beta\psi)(\kappa + \delta y + \beta\epsilon)^2 \leq 0$, the MC supply chain's profit function is concave in $p^C_A$, $r^C_A$, and $m^C_M$. According to Theorem 3.1, the first order conditions for extreme points are $\frac{\partial \pi^C}{\partial p^C_A} = 0$, $\frac{\partial \pi^C}{\partial r^C_A} = 0$, and $\frac{\partial \pi^C}{\partial m^C_M} = 0$. These equations lead to the following solutions:

$$
p^C_A = \frac{\phi(\gamma\psi - (\alpha - x\delta)\psi)}{\Phi}$$

$$
r^C_A = \frac{\phi(\gamma\psi + y^2\delta - \nu\beta\epsilon - 2\beta\delta\epsilon + \beta^2\epsilon^2 - 2\beta\kappa + 2\kappa^2\beta\epsilon)}{\Phi}$$

$$
m^C_M = \frac{\phi(\gamma - \beta\epsilon)(\gamma\psi - \gamma\phi - 2x\delta\psi)}{\Phi}$$

Proof. The Hessian matrix of the MC supply chain’s profit based on cooperative game is

$$
H_{\pi^C} = \begin{pmatrix}
\frac{\partial^2 \pi^C}{\partial p^2} & \frac{\partial^2 \pi^C}{\partial p \partial r} & \frac{\partial^2 \pi^C}{\partial p \partial m} \\
\frac{\partial^2 \pi^C}{\partial r \partial p} & \frac{\partial^2 \pi^C}{\partial r^2} & \frac{\partial^2 \pi^C}{\partial r \partial m} \\
\frac{\partial^2 \pi^C}{\partial m \partial p} & \frac{\partial^2 \pi^C}{\partial m \partial r} & \frac{\partial^2 \pi^C}{\partial m^2}
\end{pmatrix}
$$

$$
= \begin{pmatrix}
-2\beta & \gamma & \delta y + \beta\epsilon \\
\gamma & -2\psi & 0 \\
\delta y + \beta\epsilon & 0 & -\kappa - \delta y\epsilon
\end{pmatrix}
$$

From the above, $H_{\pi^C}$ is a negative definite matrix provided that $4\beta\psi - \gamma^2 > 0$ and $(\gamma^2 - 4\beta\psi)(\kappa + \delta y + \beta\epsilon)^2 \leq 0$. Thus, the supply chain’s profit function is concave in $p$, $r$, and $m$. □
Which

\[ \Phi = 2v\gamma \left( \beta \epsilon - y\delta \right) + 2\nu \left( 2y\beta \delta \epsilon - y^2\delta^2 \right) - \gamma^2\kappa + 2\nu\beta \left( 2\kappa - y\delta^2 - \delta^2 \right) \]

From the above optimal decisions, we have the following important observations.

**Proposition 3.4** If \( \gamma \) increases, \( \nu_A^{C*} \) will increase provided that \( \gamma \geq \nu \left( \beta \epsilon - y\delta \right) / \kappa \) and \( \alpha \kappa \) is a large constant; \( m_A^{C*} \) and \( w_M^{C*} \) will increase while \( \nu \left( \beta \epsilon - y\delta \right) / \kappa \leq \gamma \leq \alpha \nu \left( x\delta - \beta \epsilon \right) / \nu \).

**Proof.** If \( \gamma \geq \nu \left( \beta \epsilon - y\delta \right) / \kappa \), the denominators of \( \nu_A^{C*} \) and \( m_A^{C*} \) will decrease with the increase of \( \gamma \), while the numerator of \( \nu_A^{C*} \) will increase provided that \( \alpha \kappa + \phi \nu y\delta - \phi \nu \beta \epsilon - x\delta \kappa \geq 0 \), that is, when \( \alpha \kappa \) is a large enough constant, hence, \( \nu_A^{C*} \) will increase; The numerator of \( m_A^{C*} \) is a quadratic function respect to \( \gamma \), thus, the numerator will increase when

\[ \frac{\alpha \nu \psi - x\delta \nu \psi - (y\delta - \beta \epsilon) \psi}{\psi} \]

Hence, \( m_A^{C*} \) will increase. Because of the linear relationship to \( m_M^{C*} \), the trends of \( w_A^{C*} \) and \( \nu_A^{C*} \) are obvious. \( \square \)

The insight of Proposition 3.4 is similar to Proposition 3.1. When refund-demand sensitivity coefficient \( \gamma \) increases, in order to attract consumers, the assembler will offer a more generous refund provided that \( \gamma \geq \nu \left( \beta \epsilon - y\delta \right) / \kappa \approx 0 \) and \( \alpha \kappa \) is a large enough constant which is mild and can be satisfied in most cases. Thus, the upstream manufacturer has to increase his modularity level to compensate the downstream assembler's huge refund cost, otherwise, the cooperation in the supply chain would be disrupt.

**Proposition 3.5** If the base return quantity \( \phi \) increases, \( p_A^{C*} \) will increase if \( \kappa \) is a large enough constant; \( r_A^{C*} \) will decrease if \( 2\beta \kappa \) is large enough; \( m_A^{C*} \), \( w_A^{C*} \) and \( \nu_A^{C*} \) remain fairly constant.

**Proof.** Similar to Proof of Proposition 3.4, we skip it for brevity.

When the base return quantity \( \phi \) increases, the retail price will increase, the result is contrary to those of simultaneous-move and sequential-move games. This is due to that the cooperation increases the profit, though the demand has been declined for the high retail price.

By Embedding \( p_A^{C*} \), \( r_A^{C*} \), \( m_A^{C*} \) and \( w_M^{C*} \) into \( D_{(p,r)} \), \( \pi_A^{C*} \) and \( \pi_M^{C*} \), the market demand and the supply chain's maximum profit can be rewritten as:

\[ D^C = \frac{\beta \nu \Phi \left( \nu^2 \psi - \kappa \right)}{\Phi} + \frac{\beta \nu \left( 2\alpha \kappa - 2x\delta \kappa + y\nu \delta \phi \right)}{\Phi} + \frac{\nu \left( -\nu \beta \Phi \phi - \nu^2 \alpha \psi + \nu^2 \delta \psi \right)}{\Phi} \]

\[ \pi_{sc}^C = \left[ \alpha - \beta \nu \left( \nu r_A^{C*} - \nu \delta \left( x - \nu m_A^{C*} \right) \right) \right] \left( p_A^{C*} - \epsilon m_M^{C*} \right) - \left( \phi + \nu r_A^{C*} \right) \left( r_A^{C*} - \nu m_A^{C*} \right) - \left( \frac{1}{2} \kappa m_M^{C*} + \eta \right) \Delta_i (36) \]

In addition to the above findings, we explicitly present an item to item comparison between three different games in Table 1. As a remark, In Table 1., we present the analytical effects brought by the increase of each important parameter. From Table 1., we can see that, by considering the sufficient conditions, we are able to reveal the effects as being brought by increase of each important parameter.
4. Coordinative mechanism

4.1. Coordinative conditions

The most important performance metric for MC supply chain is profits [44]. After comparing the equilibrium results of MC supply chain in the simultaneous-move, the sequential-move and the cooperative decision cases, we have easily obtained proposition as follows (See Numerical Studies in Section 5).

Proposition 3.6 The profits the whole supply chain in the non-cooperative models are lower than the whole supply chain case. Although the strategic cooperation can effectively improve the performance of MC supply chain, when compared to the non-cooperative supply chain case. The aforementioned proposition indicates that a strategic cooperation can avoid the double marginalization effect and effectively improve the performance of MC supply chain, when compared to the non-cooperative supply chain case. Although the strategic cooperation can effectively improve the profits of the whole MC supply chain, not every supply chain member’s profits are sure to improve simultaneously, when one side suffers from the strategic cooperation, the cooperation between the chain members will not continually exist. So, to ensure cooperation, an optimal profit scheme between the module manufacturer and the customization assembler should meet the following relationships.

\[
\Delta \pi_M = \pi_{M}^{St} - \pi_{M}^{N} \geq 0 \quad (37)
\]

\[
\Delta \pi_C = \pi_{C}^{St} - \pi_{C}^{N} \geq 0 \quad (38)
\]

Where $\Delta \pi_M + \Delta \pi_C = \Delta \pi$ and $\Delta \pi$ are the module manufacturer and the customization assembler’s incremental profits, respectively. $\pi_{M}^{St}$ and $\pi_{C}^{St}$ denote the module manufacturer’s and the customization assembler’s profits in the cooperation scenario, respectively.

| Parameters | Simultaneous-move Game | Sequential-move Game | Cooperative Game |
|------------|-------------------------|----------------------|-----------------|
| $\alpha$   | $p \uparrow, r \uparrow$ | $p \uparrow, r \uparrow$ | $p \uparrow, r \uparrow$ |
| $\beta$   | $p \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ |
| $\gamma$ | $\kappa$ large enough | $r \uparrow$ | $\kappa$ large enough |
| $\delta$ | $p \downarrow, r \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ |
| $\phi$   | $p \uparrow, r \downarrow$ | $p \uparrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ | $r \uparrow, m \uparrow, w \uparrow, t \uparrow$ |
| $\psi$   | $2\beta \geq \gamma^2$ | \(2\beta \geq \gamma^2 \) | \(2\beta \geq \gamma^2 \) |
| $\psi$   | $\kappa$ large enough | $r \downarrow$ | $\kappa$ large enough |
| $\psi$   | $p \downarrow, r \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ |
| $\psi$   | $p \uparrow, r \downarrow$ | $p \uparrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ | $p \uparrow, r \downarrow, m \downarrow, w \downarrow, t \downarrow$ |
| $\kappa$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \uparrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \uparrow$ | $p \downarrow, r \downarrow, m \downarrow, w \downarrow, t \uparrow$ |
Proposition 3.7 Under the strategic cooperation, there exists at least one Pareto efficient scheme that can effectively improve the individual profits of each MC supply chain member.

This proposition tells us that both the module manufacturer and the customization assembler can gain greater profits in a strategic cooperation than in a non-cooperation setting. It should be clearly understood, however, that not all Pareto efficient schemes are accepted by each supply chain member. Both the manufacturer and the assembler will be willing to accept the Pareto efficient scheme only when each supply chain member gains more profits in the strategic cooperation than in the non-cooperation setting. Therefore, it is necessary to find an efficient profit-sharing mechanism to maximize the profits for each MC supply chain member. In the following subsection, we propose a scheme—Nash bargaining model—to optimize the profit for each MC supply chain player.

4.2. Profit-sharing scheme with bargaining power

The Nash bargaining model [45] has been widely used in many fields [46-48], here we will use the Nash bargaining model to determine the proportion of profit sharing between the module manufacturer and customization assembler.

\[ u_i(\Delta \pi_i) = (\Delta \pi_i)^{1/k_i} \]  

(39)

In this equation, \( u_i(\Delta \pi_i) \), \( i \in \{M, A\} \) denotes the manufacturer’s and assembler’s utility function, respectively. Where \( k_i (k_i > 0) \) denotes the bargaining power for the chain member \( i \). So, the system’s utility function can be derived based on the Nash bargaining power model.

\[ u_M u_A = (\Delta \pi_M)^{1/k_M} (\Delta \pi_A)^{1/k_A} \]  

(40)

Next, via maximizing the equation above subject to the constraint \( \Delta \pi_M + \Delta \pi_A = \Delta \pi \) yields

\[ \Delta \pi_M = \frac{k_M}{k_M + k_A} \Delta \pi \]  

(41)

Here, \( \frac{k_M}{k_M + k_A} \Delta \pi \) represents the proportion of the increased profits that the manufacturer gains, \( \frac{k_A}{k_M + k_A} \Delta \pi \) stands for the proportion of the increased profits that the assembler gains.

From the equations (41) and (42), we can easily find the following implications

1) A member who has a stronger power than the other party will receive a larger proportion of the increased profits and vice versa;
2) A member with sufficient/dominant bargaining power will get approximately all of the increased profits and vice versa;
3) If both parties have the same bargaining power, they will equally get the half of the increased profits.

5. Numerical studies

5.1. Comparison of Optimal Decision-making

In the following, we carry out numerical analysis to study the performance and impact of the three models, i.e. to compare upstream module manufacturer’s and downstream tailored assembler’s price, refund rate, lead time, the level of modularity, market demand and profits in MC supply chain. Suppose that we have a MC problem with the parameters given in Table 2. All the numerical analysis are conducted in Mathematica 4.0 environment running on an ordinary personal computer with a dual-core (3.20 and 3.19GHz) and 2-GB memory; the way to compute the numerical results and to draw the figures follows the standard commands in Mathematica, and we do the computations interactively with computer.

The optimal decisions and profits for the tailored assembler and module manufacturer under simultaneous-move game, sequential-move game and cooperative game are show in Table 3 respectively.
Table 2. Parameters values

| α  | β  | γ  | δ  | x  | y  | θ  | ε  | φ  | ψ  | ν  | F₁ | η  | Κ  |
|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| 500| 0.5| 0.2| 0.3| 20 | 10 | 200| 50 | 20 | 0.2| 400| 500 | 20000| 3500|

Table 3. The optimal decisions and profits

| Strategies                  | p   | r   | t   | m   | w   | D   | πₙₘ | πₘ | π₟ |
|-----------------------------|-----|-----|-----|-----|-----|-----|------|-----|-----|
| Simultaneous-move game      | 627.867 | 166.933 | 20 | 0.017 | 200.85 | 213 | 32622.6 | 22695.8 | 55318.4 |
| Sequential-move game        | 630.667 | 175.333 | 19 | 0.057 | 202.85 | 214 | 33114.1 | 22723.8 | 55837.9 |
| Cooperative game            | 589.151 | 373.009 | 13 | 0.734 | 236.70 | 276 | 39842.4 | 25819.8 | 65662.2 |

Table 4. Impacts of parameters $k_M$, $k_A$ on profit in MC chain

| $k_M$ | $k_A$ | $\Delta \pi_M$ | $\Delta \pi_A$ | $\Delta \pi$ | $\pi_M$ | $\pi_A$ | $\pi_T$ |
|-------|-------|----------------|----------------|-------------|---------|---------|---------|
| 0     | 0     | 9824.         | 9824           | 22723.     | 42938.  | 65662.  |
| 0.3   | 0.3   | 9924.         | 9824           | 23028.     | 43938.  | 66662.  |
| 0.5   | 0.5   | 9924.         | 9824           | 23028.     | 43938.  | 66662.  |
| 0.7   | 0.7   | 9924.         | 9824           | 23028.     | 43938.  | 66662.  |
| 1     | 1     | 9824.         | 9824           | 22723.     | 42938.  | 65662.  |

As show in Table 3, it is found that the higher retail prices are 630.667 and 627.867 that occur at the sequential-move game and simultaneous-move game whereas the lowest retail price is 589.151 that occurs when the assembler and the manufacturer cooperate. The high values of the retail price in the conflict cases versus the low value of the retail price in the coordination case are both well known in the literature. Now, if the upstream manufacturer is the leader, in order to reduce the cost, he will abuse his position to impose a very low level of modularity (much less than 0.1) to its downstream assembler who have consequently no choice but to mark a high retail price to compensate his assembler cost, at the same time, the customization lead time will increase (about 20 days) which will lead to a low demand in the customized market (about 213).

Similarly, we also get a comparison between the different refund rates in the different strategies. Though the assembler’s retail prices are high in the simultaneous-move and sequential-move games, in order to compensate the assembly cost, the assembler will not set a high refund rate (about 170). While in the Cooperative game, the refund rate (373.009) is much larger than in simultaneous-move game and sequential-move game, mainly because the upstream module manufacturer is willing to enhance the level of modularity (0.734) for the purpose of the maximum profit of the whole supply chain.

Table 3 compares the manufacturer’s, the assembler’s and the supply chain’s profits in the simultaneous-move, sequential-move and Cooperative Games respectively. There are two striking findings: 1) The profits (both the participants and the whole supply chain) in sequential-move game is slightly better than simultaneous-move game, 2) The profits in Cooperative game is much better than the non-cooperative game. There are mainly two explanations to these observations: 1) In the Cooperative game, the lowest retail price (589.151) will lead to the expansion of market demand (276) directly, which is much higher than in simultaneous-move game (213) and sequential-move game (214), the profits will also increase consequently. 2) The cooperation between the firms can be explored and their advantages can be given full play in the strategy of cooperative game. The upstream module manufacturer will take advantage of MP to increase the modularity level and decrease the manufacturing cost for the whole supply chain, the downstream assembler will make efforts to shorten the lead time according to customer’s needs, thus, in cooperative game, the modularity is the highest (0.734) and the lead time is the lowest (13). At the same time, the wholesale price (236.7) is higher than that of the simultaneous-move game (200.85) and the sequential-move game (202.85), which will ensure each firm’s benefits and prevents from the effect of double marginalization effectively and obtain win-win strategy.

Table 4 shows the effect of parameters $k_M$ and $k_A$ on the module manufacturer and customization assembler’s equilibrium profits in a MC supply chain. The cooperative decision modeling can lead to an increase in profits ($\Delta \pi$) with 9824.3, compared with the Stakelberg decision case. The optimal coordination
state can be achieved if the manufacturer and the assembler sanely allocate the incremental profits. It is easily to see if the manufacturer or the assembler’s bargaining power is stronger than the other party, it will derive larger proportion of the increased profits. As $k_M$ or $k_A$ increases, the total profits of the manufacturer or the assembler’s profits increases. For example, the total profits of the manufacturer is 25671.09 when $k_M$ equals 0.3, and the profits increases to 29600.81 when $k_M$ equals 0.7. The profit sharing scheme realizes only if the manufacturer and the assembler can obtain reservation profits in the sequential-move decision case. When the one party in MC supply chain sufficiently yields to the other party ($k_M = 0$ or $k_A = 0$), the mighty with stronger power will obtain the whole increased profits.

5.2. Sensitive Analysis

5.2.1 Effects on retail price

To explore the effect of each coefficient on the retail price, we use the parameters in Table 2 for study, the trends of the retail prices in different games are show in Fig. 2. As show in Fig. 2, it is found the retail prices for simultaneous-move and sequential-move game are almost the same, and the tendencies are similar to the cooperative game.

Fig. 2(a) shows the influence of demand on retail price sensitivity coefficient, the retail price decreases dramatically with $\beta$ increasing, and be stable when $\beta$ reaches to 0.6, we also find the MC supply chain can be more endurable to lowing price in the case of...
cooperative game. Fig. 2(b) allows us to see the influence of refund-demand sensitivity coefficient, retail price $\gamma$ increases up to 0.6 and then approaches the positive infinity. The result shown in Fig. 2(c) reveals the variable coefficient $\varepsilon$ has almost no influence on simultaneous-move game’s and sequential-move game’s retail price, while for the cooperative game, the retail price decreases slowly while $\varepsilon$ increases. From Fig. 2(d), the wholesale price coefficient $\theta$ has no effect on cooperative game’s retail price, but for the simultaneous-move game and sequential-move game, there is a positive moderate linear relationship between retail price and $\theta$. As shown in Fig. 2(e), the influences of return quantity coefficient $\psi$ are significant for the non-cooperative and cooperative games in the range of $\psi \leq 0.1$, while in the range of $\psi > 0.1$, the retail price almost remains stable, the jump discontinuity point in cooperative game is the zero point existing in the denominator, that has little practical effect. In Fig. 2(f), unit reusability value $\nu$ has no effect on non-cooperative games’ retail price and has no significant effect on the cooperative game. The results indicate that, when the customized market is sensitive to retail price, the supply chain has to lower retail price to consolidate the market share, meanwhile, the MC supply chain can simulate the market demand by higher $\gamma$ value.

5.2.2 Effects on refund rate

Fig. 3 shows the influence on the refund rate $r$. From Fig. 3(a) to Fig. 3(f), the refund rate in cooperative game is generally more than the two non-cooperative games. Fig. 3(a) reveals that there is an inverse correlation between the refund rate and price sensitivity coefficient $\beta$, the refund rate decreases significantly
while increases in the range of $\beta \leq 0.4$. From Fig. 3(b), the influences of $\gamma$ is notable both for the Non-cooperative and Cooperative games, refund rate $\gamma$ increases up to 0.6 and then approaches the positive infinity. As show in Fig. 3(c), the variable cost coefficient $\varepsilon$ has little influence on non-cooperative games’ refund rate, while for the cooperative game, $\varepsilon$ plummets with $\varepsilon$ increasing. In Fig. 3(d), the wholesale price coefficient $\theta$ has no effect on cooperative game’s refund rate, also, has little influence on non-cooperative games’. As show in Fig. 3(e), the refund rates of all of three games plummet in the range of $\psi \leq 0.2$. However, in the range of $\psi > 0.2$, the slope for non-cooperative games’ refund rate are relatively flat, while for the cooperative game, the refund rate begins to rebound significantly. Fig. 3(f) reveals that the unit reusability value $v$ has little effect on non-cooperative games’ refund rate, but for the cooperative game, the refund rate increases with $v$ increasing.

Hence, the customized products in cooperative game should be more attractive when the customer demand is more sensitive to the return policy. Though the refund rate is higher than the Non-cooperative supply chain, it is more profitable for the cooperative supply chain due to the larger market demand (refer to Fig. 5).

5.2.3 Effects on modularity level
see that modularity levels are proportional to the refund-demand sensitivity coefficient \( \gamma \), it reaches to 1 at the point of \( \gamma = 0.6 \) in sequential-move game, however, in cooperative game, it dramatically increases from 0.2 to 1. In Fig. 4(c), the modularity level decreases while \( \varepsilon \) increases, furthermore, the modular production dose not exist in the MC supply chain when \( \varepsilon \geq 100 \). Fig. 4(d) reveals that the wholesale price coefficient \( \Theta \) only impacts the profit sharing in the MC supply chain, not the modularity level. As show in Fig. 4(e), the modularity levels in sequential-move game and cooperative game decrease rapidly in the range of \( \psi < 0.1 \). However, in the range of \( \psi > 0.1 \), the sequential-move game’s refund rate is almost stable \( (m=0.1) \), while the Cooperative game’s refund rate decreases to 0.5 at \( \psi = 0.1 \), then rebounds to \( m=1 \) at \( \psi = 0.3 \). Fig. 4(f) reveals that, the unit reusability value \( v \) has little effect on non-cooperative games’ modularity levels. But for the cooperative game, there is a positive linear relationship between \( m \) and \( v \), the modularity level greatly increases up to 1 in the range of \( v \geq 200 \).

5.2.4 Effects on market demand
Fig. 5 reflects the effects of each individual coefficients on the market demand. From Fig. 5(a) to Fig. 5(f), we can see that, the market demands are almost the same in the two non-cooperative games but far less than in the cooperative game. As show in Fig. 5(a), under the influence of price sensitivity coefficient, the market demand drops significantly in range of $\beta \leq 0.2$. Fig. 5(b) reveals that the market demand will approaches the positive infinity when $\gamma = 0.6$. In Fig. 5(c), the variable cost coefficient $\theta$ has no influence on non-cooperative games’ market demand, but for the cooperative game, when $\theta$ increases, the market demand decreases and then increases, but the fluctuation range is small. From Fig. 5(d), the market demand has inverse relationship with the basic return quantity $\phi$. As Fig. 5(e) illustrates, when the influence of the return quantity sensitivity coefficient $\psi$ on customer’s choice increases, the market demand decreases, this is mainly due to the fact that the refund rate provided by the module manufacturer is low, in addition, the jump discontinuity point in Fig. 5(e) is the zero point existing in the denominator, it has little practical effect. Fig. 5(f) reveals the unit reusability value $\nu$ has little effect on market demand.

5.2.5 Effects on lead time

Fig. 6 describes the influence on lead time. We can see from Fig. 6 that the lead time in simultaneous-move game is very long and almost steady in any case, while in the sequential-move game, the lead time has a tendency to be relatively short. However, for the cooperative game, the lead time is the shortest and remains unstable, it means through cooperation supply chain could greatly minimize lead time, but hardly control it to some extent.

Fig. 6(a) shows that the lead time has positive relationship with the price sensitivity coefficient $\beta$. The up trend of sequential-move game’s lead time is obvious in range of $\beta \leq 0.1$, then remains stable. While in the cooperative game, the lead time remains at 10 and does not increase until $\beta=0.4$. Fig. 6(b) shows a negative relation between lead time and the refund-demand sensitivity coefficient $\gamma$. However, in cooperative game, it reaches to the minimum value (10) at the point of $\gamma = 0.2$ with the most significant trend, it also achieves stability at the point of $\gamma = 0.6$ in sequential-move game. In Fig. 6(c), the lead time increases with $\epsilon$ increasing, and reaching the maximum points at $\epsilon = 100$. Fig. 6(d) reveals that the basic return quantity $\phi$ has no effect on lead time. As show in Fig. 6(e), the
lead times in sequential-move game and cooperative game increase rapidly when \( \psi \) is not larger than 0.1. However, in the range of \( \psi > 0.1 \), the sequential-move game’s lead time almost keeps stable, while for cooperative game’s lead time, it starts to decrease at the point of \( \psi = 0.1 \) from the maximum value (15) to the minimum value (10). Fig. 6(f) reveals that the unit reusability value \( v \) has little effect on non-cooperative games’ lead times, but for the cooperative game, there is a positive linear relationship between \( t \) and \( v \), the lead time decreases markedly in the range of \( v \geq 200 \) until \( t = 10 \).

6. Conclusion and future research

In this paper, we have investigated the competition and cooperation between the upstream module manufacturer and the downstream customized assembler under the MC supply chain scenario. Through employing the game theory, we have identified the optimal pricing, modularity level, return policy and lead time in three types of decision-makings. In addition, coordination mechanism is design to cooperate in MC supply chain via profit-sharing scheme. Finally, we have used numerical analysis and gained some insights into how different parameters affect the optimal decisions.
We have found that retail price, refund rate and market demand in competition environment (simultaneous-move and sequential-move games) are almost the same. However, the refund rate for MC supply chain under cooperation setting (cooperative game) is larger than that under non-cooperative setting, it is more profitable for the whole supply chain due to the larger market demand. The modularity level in simultaneous-move game is very low and almost steady, while in the sequential-move game, the modularity level has been increased significantly, however, the highest modularity level occurs in the cooperative environment. The lead time in simultaneous-move game is very long and almost steady, while in the sequential-move game, the lead time has a tendency to be short but relatively flat. However, the cooperative MC supply chain can greatly reduce lead time, which is important for MC supply chain to quickly respond to market change and remain competitive advantage.

We also examined the uncertainty issue associated with MC implementation under supply chain through sensitive analysis. It appears that different optimal decisions will result depending on the factor change. we have found that the variable cost and unit reusability value have little effect on the optimal decision in competition settings, while in the cooperative one, the influence of wholesale price is not significant. At the same time, we have revealed the price sensitivity coefficient $\beta$ and the refund-demand sensitivity coefficient $\gamma$ are influential both for the competition and cooperative settings, thus, the MC supply chain should pay more attention to the pricing strategy and refund policy. What’s more, we also have found that the MC supply chain only employ cooperative strategy, which is helpful in achieving Pareto improvement for the members along MC supply chain.

This work reveals some promising areas where one could place more efforts in the future. More sophisticated aspects in MC supply chain be added into the model. For example, risk issue of the upstream and downstream firms may vary in different decision-making. The risk attitude of MC supply chain member has influence on results, thus risk preference could be applied into this framework.

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References

1. B. J. Pine. Mass customization: the new frontier in business competition. Harvard Business Press, 1999.
2. J. Xu, Q. Liu, R. Wang. A class of multi-objective supply chain networks optimal model under random fuzzy environment and its application to the industry of Chinese liquor. Information Sciences, 178(2008): 2022-2043.
3. M. Shan, X. Hua, Z. Chen. The research of product configuration for mass customization. Machinery Design & Manufacture, 10(2007): 89.
4. S. W. Chiou. A non-smooth optimization model for a two-tiered supply chain network. Information Sciences, 177(2007): 5754-5762.
5. S. E. Lee, J. C. Chen. Mass customization Methodology for an Apparel Industry with a Future. Journal of industry technology Journal of, 16(1999): 2-8.
6. H. T. Yeung, T. M. Choi, C. H. Chiu. Innovative mass customization in the fashion industry, Innovative quick response programs in logistics and supply chain management. Springer Berlin Heidelberg, pp. 423-454, 2010.
7. S. H. Pasandideh, S. T. Niaki, K. Asadi. Bi-objective optimization of a multi-product multi-period three-echelon supply chain problem under uncertain environments: NSGA-II and NRGA. Information Sciences, 292(2015): 57-74.
8. N. Liu, et al. Optimal pricing, modularity, and return policy under mass customization. Systems, Man and Cybernetics, Part A: Systems and Humans, IEEE Transactions on, 42(2012): 604-614.
9. D. Wu, D. D. Wu, Y. Zhang. Supply chain outsourcing risk using an integrated stochastic-fuzzy optimization approach. Information Sciences, 235(2013): 242-258.
10. R. Dewan, J. Bing, A. Seidmann. Product customization and price competition on the Internet. Management Science, 49(2003)1055-1070
11. N. Kamali, L. Suzanne, Mass Customization: On - line Consumer Involvement in Product Design. Journal of Computer - Mediated Communication, 7(2002) 110-123.
12. X. Wan, B. Dan, Y. Jing. On Product Configuration Based on Customer Requirement Templates under Online Mass Customization, Industry Engineering Journal, 4(2010)15-16
13. I. Konstantaras, K. Skouri, S. Papachristos. Optimal pricing, return and modular design policy for build-to-order (BTO) products in a two parties supply chain system. IMA Journal of Management Mathematics, 22(2011): 1-12
14. S. K. Mukhopadhyay, S. Robert. Optimal return policy and modular design for build-to-order products. Journal of Operations Management, 23(2005)496-506.
15. S. L. Wood. Remote purchase environments: the influence of return policy leniency on two-stage decision processes. Journal of Marketing Research, 38(2001) 157-169.
16. Z. M. Bi, W. J. Zhang. Modularity technology in manufacturing: taxonomy and issues. The International Journal of Advanced Manufacturing Technology, 18(2001)381-390.
17. R. Sanchez. Using modularity to manage the interactions of technical and industrial design. Academic Review, 2(2002) 8-19.
18. P. Desai, et al. Product differentiation and commonality in design: Balancing revenue and cost drivers, Management Science, 47(2001)37-51
19. P. Gu, et al. An integrated modular design methodology for life-cycle engineering. CIRP Annals-Manufacturing Technology, 46(1997)71-74.
20. R.L. Dou, C. Zong, G.F. Nan. Multi-stage interactive genetic algorithm for collaborative product customization [J]. Knowledge Based System, DOI: 10.1016/j.knosys.10(2015)
21. A. M. Shaik, V. Rao, C. S. Rao. Development of modular manufacturing systems—a review. The International Journal of Advanced Manufacturing Technology, 58(2015)789-802
22. S. Da, D. B. Giovani, F. S. Fogliatto. Mass customization: Literature review and research directions. International journal of production economics, 72(2001)1-13.
23. F. T. Piller, M. S. Christof. Mass customization: four approaches to deliver customized products and services with mass production efficiency. Engineering Management Conference, 2002. IEMC’02. 2002 IEEE International.
24. J. Yang, D. H. Kincade, J. H. Chen. Types of apparel mass customization and levels of modularity and variety: application of the theory of inventive problem solving. Clothing and Textiles Research Journal , 3(2015)199-212
25. M. Zhang, X. Zhao, Y. Qi. The effects of organizational flatness, coordination, and product modularity on mass customization capability. International Journal of Production Economics , 23(2014)145-155
26. E. Mavridou, D. D. Kehagias, D. Tzovaras, G. Hassapis. Mining affective needs of automotive industry customers for building a mass-customization recommender system . Journal of Intelligent Manufacturing, 2(2013)251-265
27. X. F. Shao. Integrated product and channel decision in mass customization . IEEE Transactions on Engineering Management, 1(2013)30-45
28. M. Y. Jaber, S. K. Goyal. Coordinating a three-level supply chain with multiple suppliers, a vendor and multiple buyers. International Journal of Production Economics, 116(2008)95-103
29. G. Q. Huang, X. Y. Zhang, V. H. Lo. Integrated configuration of platform products and supply chains for mass customization: a game-theoretic approach. Engineering Management, IEEE Transactions on, 54(2007)156-171
30. A. Alptekinoglu, C. J. Corbett. Mass customization vs. mass production: Variety and price competition, Mass customization vs. mass production: Variety and price competition. Manufacturing & Service Operations Management, 10(2008)204-217.
31. N. Xia, R. Sampath. Standard vs. custom products: variety, lead time, and price competition. Marketing Science, 29(2009)887-900
32. J. Xie, J. C. Wei. Coordinating advertising and pricing in a manufacturer-retailer channel. European Journal of Operational Research, 197(2009)785-791.
33. H. Mendelson, A. K. Parfakturk. Product-line competition: Customization vs. Proliferation, Management Science. 54(2008)2039-2053.
34. D. P. Song. Optimal integrated ordering and production policy in a supply chain with stochastic lead-time, processing-time, and demand. Automatic Control, IEEE Transactions on, 54(2009)2027-2041.
35. G. Dobson, C. A. Yano. Product offering, pricing, and make-to-stock/ make-to-order decisions with shared capacity. Production and Operations Management, 11(2002): 293-312.
36. Y. Chen, G. Iyer. Research note consumer addressability and customized pricing. Marketing Science, 21(2002)97-208.
37. B. Liu, et al. Supply-chain coordination with combined contract for a short-life-cycle product. Systems, Man and Cybernetics, Part A: Systems and Humans, IEEE Transactions on, 36(2006) 53-61.
38. N. B. Syam, N. Kumar. On customized goods, standard goods, and competition. Marketing Science, 25(2006)525-537.
39. A. Kumar. Mass customization: metrics and modularity. International Journal of Flexible Manufacturing Systems, 16(2004)287-311.
40. X. Meng, Z. Jiang, G. Q. Huang. On the module identification for product family development. The International Journal of Advanced Manufacturing Technology, 35(2007)26-40.
41. J. H. Mikkola, G. Gassmann. Managing modularity of product architectures: toward an integrated theory. Engineering Management, IEEE Transactions on, 50(2003)204-218.
42. M. A. Schilling. Toward a general modular systems theory and its application to interfirm product modularity. Academy of management review, 25(2000)312-334.
43. C. Shapiro, H. Varian. Information rules. Harvard Business Press, 1998.
44. S. Apak; O. Vayvay, O. Feyzioglu. A decision making model for the evaluation of supply chain execution and management systems. International Journal of Computational Intelligence Systems, 2(2013)293-306.
45. J. Nash. The bargaining problem. Econometrica, 18(1950)155-162.
46. R. Yan. Cooperative advertising, pricing strategy and firm performance in the e-marketing age. Journal of the Academy of Marketing Science, 38(2009) 510-519.
47. P. Chow, T. Choi, T. Cheng, T. Cheng. Impacts of minimum order quantity on a quick response supply chain. IEEE Transactions on Systems, Man, and Cybernetics, 42(2012)868-879