Long-range Cooper pair splitter with high entanglement production rate

Wei Chen¹, D. N. Shi¹ & D. Y. Xing²,³

¹College of Science, Nanjing University of Aeronautics and Astronautics, Nanjing 210016, China, ²National Laboratory of Solid State Microstructures and Department of Physics, Nanjing University, Nanjing 210093, China, ³Collaborative Innovation Center of Advanced Microstructures.

Cooper pairs in the superconductor are a natural source of spin entanglement. The existing proposals of the Cooper pair splitter can only realize a low efficiency of entanglement production, and its size is constrained by the superconducting coherence length. Here we show that a long-range Cooper pair splitter can be implemented in a normal metal-superconductor-normal metal (NSN) junction by driving a supercurrent in the S. The supercurrent results in a band gap modification of the S, which significantly enhances the crossed Andreev reflection (CAR) of the NSN junction and simultaneously quenches its elastic cotunneling. Therefore, a high entanglement production rate close to its saturation value can be achieved by the inverse CAR. Interestingly, in addition to the conventional entangled electron states between opposite energy levels, novel entangled states with equal energy can also be induced in our proposal.

Generation and detection of the electron entanglement in solid state physics have attracted great scientific interest, for the prospect of large-scale implementation of quantum information and computation schemes¹. The conventional BCS superconductor are considered as a natural source of spin entanglement²,³, for the Cooper pair in the superconductor can break up into two nonlocal entangled electrons that enter into different normal terminals via the crossed Andreev reflection (CAR)⁴,⁵. Recently, the feasibility of a Cooper pair splitter has been demonstrated by the nonlocal conductance⁶ and noise⁷ measurement. The finite bias Cooper pair splitting⁸ and high purity of nonlocal transport by CAR⁹ were also reported in the quantum dots based splitter. However, the main limitation of the existing proposals is that the entanglement production rate is still at low level, even when the competitive elastic cotunneling (EC) process is filtered out⁹,¹²–¹⁵. In order to manipulate and probe entangled states⁹,¹²–¹⁵, the entanglement production rate demands well improvement. Another constraint on a conventional Cooper pair splitter is that the superconductor size \( L \), the distance between two normal metal-superconductor (NS) interfaces, cannot strongly exceed the superconducting coherence length \( \xi_0 = \frac{\hbar v_F}{2\pi D} \). A solution of such a geometric constraint will greatly facilitate the fabrication of the splitter.

In this paper, we show that both the problems can be solved with the use of a three-terminal NSN junction by driving a supercurrent in the S along the junction, as sketched in Fig. 1(a). The supercurrent results in opposite shifts of energy gaps for the electron-like and hole-like quasiparticles, as shown in Fig. 1(b). When an electron is incident to the S within the energy window (referred as the CAR window) between the two modified gaps, the hole-like quasiparticle is able to propagate freely in the S, supporting a long-range CAR, while the electron-like quasiparticle decays as usual, leading to a suppression of EC. Therefore, the probability of CAR gets significantly enhanced within the CAR window and oscillates with \( L \). By investigating the entangled states via the inverse CAR process non-perturbatively, we find that there exist two types of spin singlet states, with the entangled electron pair possessing either opposite or equal energies relative to the chemical potential of the S. The total entanglement production rate depends solely on the CAR probability and a high rate close to its saturation value can be achieved.

Long-range CAR. To be specific, we first analyze the CAR in a nanowire NSN junction as shown in Fig. 1(a), where an effective pair potential is induced in the S region due to the proximity effect of the s-wave superconductor. When a supercurrent \( I_s \) is driven in the S, the effective order parameter in the nanowire takes the form of \( \Delta e^{i\alpha} \). The Cooper pair momentum \( 2q \) can be tuned by the supercurrent through \( q = \frac{I_s}{\xi_0} \) with \( I_s = I_s/c \) normalized by its critical value \( I_c \). The whole system can be well described by the Bogoliubov-de Gennes Hamiltonian as
interfaces, which can be tuned by gates $D$. The wave functions as $(\psi_e)^2$ is the chemical potential, and the scattering amplitudes $a_1, a_2, b_1, b_2$ denote the AR, CAR, normal reflection, and EC, respectively, as shown in Fig. 1(b).

All the scattering amplitudes are solved through the boundary conditions of $\psi_N = \psi_S$ and $\psi_S = \psi_N$ at two NS interfaces, with the “$+$” and the index $j = (1, 2)$ corresponding to the interfaces at $x = 0$ and $L$, respectively. The dimensionless barrier strength is defined as $Z_j = m U_j / (4 k_0)$. As the right NS interface is transparent ($Z_2 = 0$), the CAR amplitude takes a simple form as

$$a_2 = \frac{i \sin \frac{\delta_j f(\psi_j)}{\theta_j} Z_1}{f(\psi_1) f(\psi_2)} Z_2 - g(\psi_1) g(\psi_2)(1 + Z_2^2),$$

where the auxiliary functions are defined by $f(x) = \sin(\sqrt{2} x)$ and $g(x) = \sin(\sqrt{2} x - x)$ with $L = L_0 / \xi_0$, and the energy dependent phases are defined by $\psi_{1,2} = \cos \theta_j$ for $\omega_j \leq 1$ and $\psi_{1,2} = -i \cosh \theta_j$ for $\omega_j > 1$.

As $E$ is within the CAR window, exponential factors $\beta_\pm$ and $\beta_- \pm \beta_-$ in Eq. (2) take imaginary and real values, respectively, corresponding to an evanescent wave of the electron-like quasiparticle in the $+k_F$ branch and a free wave of the hole-like quasiparticle in the $-k_F$ branch. For $Z_2 = 0$, since there is no branch-crossing scattering at the right interface, propagations of the electron-like and hole-like quasiparticles directly contribute to the EC and CAR processes, respectively. In this case, there exists only the CAR process in the long-range limit $L > \xi_0$. The numerical results of the CAR probability $A_2 = |a_2|^2$ as a function of $i_j$ and $E$ is plotted in Fig. 2(a). One can see that there is a notable region confined by the boundary approximately described by $E/\Delta = 1 \pm i_0$, where the CAR gets effectively enhanced. At the resonant energy levels, the CAR probability can reach a high value of 38%. In Fig. 2(b), we compare the CAR probability $A_2$ and EC probability $B_2 = |b_2|^2$ in the absence and presence...
of the supercurrent. For a usual NSN junction of $i_s = 0$, both CAR and EC processes are suppressed within the initial gap $\Delta$ due to the subgap decay of the normal and anomalous propagators in the S region, while EC dominates the nonlocal transport above the gap. Impressively, when a supercurrent $i_s = 0.5$ is driven, the long-range CAR occurs within the CAR window $E/\Delta \in (0.5, 1.5)$, with the EC being quenched below the modified gap $1.5\Delta$. This is a new kind of energy filtering effect, which occurs in the S, in contrast to the previous proposal in which the energy filtering is enforced in the normal leads and a large mismatch of Fermi velocities is inevitable\(^{14,15}\).

Next, we investigate the anomalous dependence of the CAR probability on $L$ of the S region. Within the CAR window, $A_2$ and $B_2$ as functions of $L$ are presented in Fig. 3(a). In the absence of supercurrent, $A_2$ first increases with $L$ and then rapidly decreases, while $B_2$ monotonically decays with $L$, as known in the usual case. As a supercurrent is driven, while the result of $B_2$ changes little, the situation for $A_2$ is quite different. With increasing $L$, $A_2$ first increases and then exhibits an oscillatory behavior due to the interference between two NS interfaces. In the large $L$ limit, we have $g(\phi_i)/f(\phi_i) \approx e^{\phi_i}$ within the CAR window, so that the CAR amplitude in Eq. (3) reduces to $A_2 = i\sin \phi Z_i\sqrt{f(\phi_i)Z_i^2 - e^{\phi_i}}g(\phi_i)(1 + Z_i^2)$, which corresponds to an oscillation period of $L_0 = \pi \xi_0 / \sinh(\phi_i)$. Under the condition of $Z_2 = 0$, the scattering between the $\pm k_F$ branches at the right NS interface is absent, so that the oscillation period is on a scale of $\xi_0$. The result for finite $Z_2$ is shown in Fig. 3(b). In this case, the branch-crossing scattering can take place at the right NS interface, so that for $L \sim \xi_0$, $A_2$ and $B_2$ exhibit fast oscillations with the period comparable with $1/k_F$. As $L$ gets larger, the propagation of quasiparticles around $+k_F$ branch cannot survive after walking such a long distance. Therefore, the fast oscillations disappear and the interference is contributed again by the free waves around $-k_F$. Due to the branch-crossing scattering at the right NS interface, the hole-like quasiparticle can now be transferred into an electron in the right lead, resulting in a finite EC probability. However, it can be shown that the ratio of the EC probability to the CAR one approximates to $B_2/A_2 = Z_2^2/(1 + Z_2^2)$ for an NSN junction of large $L$, so that the nonlocal transport is always dominated by the CAR for small $Z_2$. On the other hand, in the tunneling limit of $Z_2 \gg 1$, the two nonlocal processes cancel each other out, consistent with the previous report\(^{36}\).

By applying a negative bias voltage $eV < \Delta(1 - i_s, 1 + i_s)$ on the left lead while keeping the S and the right lead grounded as shown in Fig. 1(a), the anomalous differential conductance within the CAR window is equal to $G_2/G_0 = A_2/(1 + Z_2^2)$ with $G_0 = e^2/h$ the unit conductance (the positive direction of current is from the right lead into the S). The positive nonlocal conductance manifests a CAR-dominant nonlocal transport. The dependence of $Z_2$ on the gate voltage $V_{G2}$ can be calibrated through the normal state transport beforehand, so that the CAR probability can be measured directly by conductance $G_2$.

**Entanglement generation via inverse CAR.** By imposing a positive bias voltage ($eV < 0$) on the left lead and reversing the direction of the supercurrent, the Cooper pair can break up into two nonlocal spin entangled electrons. For the high-efficiency inverse CAR, the entangled state should be analyzed non-perturbatively. We start with the many-body state of incident holes occupying the energy window from the Fermi level to $|eV|$ in the left N region as $|\Psi_{in}\rangle = \Pi_{j < E_{F/L,E_{L,E}}}|h_j\rangle|0\rangle$, where $h_{j,L,E}$ generates an incident hole in the left lead with energy $E$ and spin $\sigma(= \uparrow, \downarrow)$, and the vacuum state $|0\rangle$ represents the Fermi sea filled up to $E = 0$ in all NSN regions. The incident and outgoing waves are related to each other via scattering coefficients as\(^{27,29}\)

$$
\gamma_{\sigma L}^{\uparrow,\downarrow} = b_{\sigma L}^{\uparrow,\downarrow}a_{\sigma L}^{\uparrow,\downarrow} + a_{\sigma L}^{\uparrow,\downarrow}b_{\sigma L}^{\uparrow,\downarrow},
$$

where $b_{\sigma L}^{\uparrow,\downarrow}$ are the operators of the outgoing hole and electron in lead $x(= L, R)$, respectively, with the energy index omitted, and the scattering amplitudes correspond to those in Eq. (2), except that the superscript denote the hole incident case. Substituting Eq. (4) into the expression of $|\Psi_{in}\rangle$, one arrives at the outgoing state of quasiparticles. Then the entangled state between electrons can be obtained by redefining a new vacuum state $|\tilde{0}\rangle$, which is related to the original one through $|0\rangle = \Pi e^{<E_{F/L,E_{L,E}}} |\tilde{0}\rangle$, and by performing a particle-hole transformation as $\gamma_{\sigma L}^{\uparrow,\downarrow} = c_{\sigma L}^{\uparrow,\downarrow} e^{\sigma_{L,E}^{\uparrow,\downarrow}}$, the many-body outgoing state can be obtained as

$$
|\Psi_{out}\rangle = \Pi_{0 < E_{F/L,E}} (|E\rangle + \kappa |\tilde{E}\rangle + |0\rangle),
$$

$$
|E\rangle = \frac{\sqrt{2}}{2} \left( c_{\sigma L}^{\uparrow,\downarrow} e_{\sigma L}^{\uparrow,\downarrow} - c_{\sigma L}^{\uparrow,\downarrow} e_{\sigma L}^{\uparrow,\downarrow} \right) |0\rangle,
$$

$$
|\tilde{E}\rangle = \frac{\sqrt{2}}{2} \left( c_{\sigma L}^{\uparrow,\downarrow} e_{\sigma L}^{\uparrow,\downarrow} - c_{\sigma L}^{\uparrow,\downarrow} e_{\sigma L}^{\uparrow,\downarrow} \right) |0\rangle,
$$

where $|E\rangle$ and $|\tilde{E}\rangle$ are two kinds of nonlocal spin singlet states induced by the inverse CAR with amplitude $\kappa = -2a_{\sigma L}^{\uparrow,\downarrow}(-E)b_{\sigma L}^{\uparrow,\downarrow}(-E)$ and $\tilde{\kappa} = \sqrt{2}a_{\sigma L}^{\uparrow,\downarrow}(-E)a_{\sigma L}^{\downarrow,\uparrow}(-E)$, respectively, and $|0\rangle$ includes the other many-body scattering states, such as the local entangled state and product states (Supplementary Information). During the derivation

---

**Figure 3** | The probabilities of CAR and EC as functions of $L$ for (a) $Z_2 = 0$ and (b) $Z_2 = 0.8$. The relevant parameters are set as $Z_1 = 1.25, E/\Delta = 0.8, k_F = 100/\xi_0$.  

---

**References:**\(^{14,15,27,29}\)
of Eq. (5), we have taken into account the particle-hole symmetry of the scattering matrix, and expressed the state with the scattering amplitudes in the electron incident case.

|\begin{align*}
  \langle \epsilon \rangle & \text{ is the usual nonlocal entangled state generated by the CAR, for which the two entangled electrons have opposite energies relative to } E_{\text{Fermi}}, \text{ as shown in the left panel of Fig. 4(a). Since the CAR is an elastic process, the total energy of the two electrons is conserved during the pair breaking. We note that the amplitude } \kappa \text{ reduces to } \\
  \sqrt{2}\zeta_1^2 \text{ in the tunneling limit of } b'_1=1, \text{ consistent with the result in previous literatures}\text{.}
\end{align*}\]

|\begin{align*}
  \langle \epsilon_1 \rangle \text{ is the anomalous entangled state in which the two entangled electrons have the same energy } E, \text{ as shown in the right panel of Fig. 4(a), which is a natural result obtained in the present non-perturbative approach. From a physical point of view, the coincidence of the AR and CAR processes first results in a double electron occupation at the } - E \text{ energy level, freezing out the spin freedom therein; then a nonlocal entangled state is induced for the electron pair with equal energy } E \text{ and opposite spins. Such a nonlocal entangled state has never been discussed before, since in the previous consideration, both } \alpha_1 \text{ and } \alpha_2 \text{ are very small in the tunneling regime, and } \kappa \text{ becomes a negligible higher-order correction}\text{.}
\end{align*}\]

Given that tunnel attempts in a unit energy interval occur with a frequency 1/h (h is the Plank constant)\textsuperscript{29,41}, the differential production rate of nonlocal entanglement can be calculated by

\[ P(EV) = 2A_2 \left( 1 - \frac{1 + 2Z_2^2}{1 + Z_2^2} A_2 \right) / h, \]

in the CAR window for the Cooper pair splitter, which is determined solely by the CAR probability. In the case of } Z_2 = 0, \text{ it is simplified to } P = 2(1 - A_2)A_2 / h, \text{ indicating that a saturation value } P = 0.5 / h \text{ can be achieved at } A_2 = 0.5. \text{ It turns out that the entanglement production rate } P \text{ is not a monotonic increasing function of the CAR probability. Only in the tunnel limit, } P \text{ increases monotonously with } A_2 \text{ because of } A_2 < 1. \text{ The numerical result of } P \text{ as a function of the bias voltage } EV \text{ is shown in Fig. 4(b). When the right NS interface is transparent, } P \text{ can approach its saturation value at the resonant energy levels within the CAR window, indicating that an ideal entangler can be implemented in our proposal. Although finite } Z_2 \text{ may suppress the entanglement production rate, large values of } P \text{ can be obtained even for a stronger barrier } Z_2 = 1, \text{ as shown in Fig. 4(b).}

The nonlocal spin entanglement of states |\epsilon_1\rangle \text{ and } |\epsilon_2\rangle \text{ can be demonstrated through either the violation of the Bell-inequality}\textsuperscript{25–32} \text{ or a well-designed spintronic quantum eraser}\textsuperscript{33,34}. \text{ Both schemes can be achieved by the spin resolved current correlation measurement. In the optimal case of } Z_2 = 0, \text{ the nonlocal spin correlation is purely contributed by } |\epsilon_1\rangle \text{ and } |\epsilon_2\rangle. \text{ In the case of } Z_2 \neq 0, \text{ the signal of entanglement will get weakened since the intervention of EC contributes an opposite current; nevertheless, provided that the CAR dominates the nonlocal transport in the CAR window, the signal of entanglement is always extractable. Moreover, the equal-energy entangled state } |\epsilon_2\rangle \text{ can also be probed by the bunching behavior in a beam splitter setup}\textsuperscript{35}, \text{ in consideration of the orbital wave function of the singlet state being symmetric.}

**Discussions**

Finally, we discuss the experimental realization of our proposal. The long-range Cooper pair splitter in Fig. 1(a) possesses the same configuration as those in the experiments reported in Refs. 6, 7, 9, 11, so that it can be implemented by the existing technology. Since no quantum dot embedded in the nanowire needs to be fabricated, more kinds of nanowires can be adopted to build the NSN junction. A key point is that there needs to be a supercurrent flowing along the junction, which can be driven by imposing a constant current on the S or by utilizing a magnetic flux in a superconducting loop. Possible renormalization of the Fermi velocity due to the superconducting proximity effect can be compensated by a back gate. In order to realize an entangler with high efficiency and extract pure signal of entanglement, the interface barriers \text{Z}_2 \text{ must be carefully tuned by gate voltages } V_{\text{g1,2}}. \text{ The optimal choice corresponding to the bias voltage configuration in Fig. 1(a) is found to be } Z_1\epsilon(1,2) \text{ and } Z_2 = 0, \text{ which can be realized in the experiment}\textsuperscript{7}.\text{ }

---

1. Nielsen, M. A. & Chuang, I. L. Quantum Computation and Quantum Information (Cambridge University Press, Cambridge, England, 2000).
2. Recher, P., Sukhorukov, E. V. & Loss, D. Andreev tunneling, Coulomb blockade, and resonant transport of nonlocal spin-entangled electrons. Phys. Rev. B 63, 165314 (2001).
3. Losovik, G. R., Martin, T. & Blatter, G. Electronic entanglement in the vicinity of a superconductor. Eur. Phys. J. B 24, 287 (2001).
4. Byers, J. M. & Flatté, M. E. Probing Spatial Correlations with Nanoscale Two-Contact Tunneling. Phys. Rev. Lett. 74, 306 (1995).
5. Deutscher, G. & Feinberg, D. Coupling superconducting-ferromagnetic point contacts by Andreev reflections. Appl. Phys. Lett. 76, 487 (2000).
6. Hofstetter, L., Csonka, S., Nygård, J., & Schönberger, C. Cooper pair splitter realized in a two-quantum-dot Y-junction. Nature (London) 461, 960 (2009).
7. Herrmann, L. G., Portier, F., Roche, P., Yeyati, A. L., Kontos, T. & Strunk, C. Carbon Nanotubes as Cooper-Pair Beam Splitters. Phys. Rev. Lett. 104, 026801 (2010).
8. Wei, J. & Chandrasekhar, V. Positive noise cross-correlation in hybrid superconducting and normal-metal three-terminal devices. Nat. Phys. 6, 490 (2010).
9. Das, A., Ronen, Y., Heiblum, M., Mahalu, D., Kretinin, A. V. & Shtrikman, H. High-efficiency Cooper pair splitting demonstrated by two-particle conductance resonance and positive noise cross-correlation. Nat. Commun. 3, 1165 (2012).
10. Hofstetter, L., Csonka, S., Baumgartner, A., Fülöp, G., D’Hollony, S., Nygård, J. & Schönberger, C. Finite-Bias Cooper Pair Splitting. Phys. Rev. Lett. 107, 136801 (2011).
11. Schindele, J., Baumgartner, A. & Schönberger, C. Near-Unity Cooper Pair Splitting Efficiency. Phys. Rev. Lett. 109, 157002 (2012).
12. Linder, J., Zareyan, M. & Sudbo, A. Spin-switch effect from crossed Andreev reflection in superconducting graphene spin valves. Phys. Rev. B 80, 041531 (2009).
13. Linder, J. & Yokoyama, T. Cooper pair splitting demonstrated by two-particle conductance resonance and positive noise cross-correlation. Phys. Rev. B 89, 020504(R) (2014).
14. Cayssol, J. Crossed Andreev Reflection in a Graphene Bipolarisator. Phys. Rev. Lett. 100, 147001 (2008).
15. Veldhorst, M. & Brinkman, A. Nonlocal Cooper Pair Splitting in a pSn Junction. Phys. Rev. Lett. 105, 107002 (2010).
25. Kawabata, S. Test of Bell's Inequality using the Spin Filter Effect in Ferromagnetic

24. Clauser, J. F., Horne, M. A., Shimony, A. & Holt, R. A. Proposed Experiment to

23. Bell, J. S. On the Problem of Hidden Variables in Quantum Mechanics.

22. Bell, J. S. On the Einstein Podolsky Rosen Paradox.

26. Chtchelkatchev, N. M., Blatter, G., Lesovik, G. B. & Martin, T. Bell inequalities and

21. Reinthaler, R. W. Recher, P. & Hankiewicz, E. M. Proposal for an All-Electrical

19. Herrera, W. J., Levy Yeyati, A. & Martin-Rodero, A. Long-range crossed Andreev

18. Golubev, D. S. & Zaikin, A. D. Non-local Andreev reflection under ac bias.

17. Yeyati, A., Levy, Bergeret, F. S., Martin-Rodero, A. & Klapwijk, T. M. Entangled

16. Chen, W., Shen, R., Sheng, L., Wang, B. G. & Xing, D. Y. Resonant nonlocal

15. Burkard, G., Loss, D. & Sukhorukov, E. V. Noise of entangled electrons: Bunching

14. Falci, G., Feinberg, D. & Hekking, F. W. J. Correlated tunneling into a superconductor in a multiprobe hybrid structure. *Europhys. Lett.* 54, 255 (2001).

13. Romito, A., Aicea, J., Refael, G. & von Oppen, F. Manipulating Majorana fermions using supercurrents. *Phys. Rev. B* 85, 020502(R) (2012).

12. Chen, W., Gong, M., Shen, R. & Xing, D. Y. Detecting Fulde-Ferrell superconductors by an Andreev interferometer. *New J. Phys.* 16 083024 (2014).

11. Blonder, G. E., Tinkham, M. & Klapwijk, T. M. Transition from metallic to tunneling regimes in superconducting micro-constrictions: Excess current, charge imbalance, and supercurrent conversion. *Phys. Rev. B* 25, 4515 (1982).

10. Prada, E. & Sols, F. Entangled electron current through finite size normal-superconductor tunneling structures. *Eur. Phys. J. B* 40, 379 (2004).

9. Levitov, L. S. & Lesovik, G. B. Charge distribution in quantum spin Hall systems. *JETP Lett.* 87, 026805 (2013).

8. Braunecker, B., Burset, P. & Levy Yeyati, A. Entanglement Detection from Competing financial interests: The authors declare no competing financial interests.

7. How to cite this article: Chen, W., Shi, D.N. & Xing, D.Y. Long-range Cooper pair splitter with high entanglement production rate. *Sci. Rep.* 5, 7607; DOI:10.1038/srep07607 (2015).

6. This work is licensed under a Creative Commons Attribution 4.0 International License. The images or other third party material in this article are included in the article's Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder in order to reproduce the material. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/

5. We would like to thank A. Baumgartner, M. Heiblum, Jing-Min Hou, Ming Gong, Zheng-Yuan Xue and Tao Zhou for helpful discussions. This work is supported by the State Key Program for Basic Researches of China under Grant No. 2011CB922103, and by the National Natural Science Foundation of China under Grants No. 11174125, No. 91021003 and No. 11374159. Wei Chen is also supported by the Project funded by China Postdoctoral Science Foundation under Grant No. 2014M560419.

4. The authors declare no competing financial interests.

3. Additional information

2. Supplementary information accompanies this paper at http://www.nature.com/

1. Scientific reports

Acknowledgments

Author contributions

W.C. conceived the project and performed the calculations. W.C. and D.Y.X. wrote the manuscript. All authors discussed the results and reviewed the manuscript.

Additional information

The views and opinions expressed herein do not necessarily reflect those of the National Science Foundation or any other entity.

Competing financial interests: The authors declare no competing financial interests.

How to cite this article: Chen, W., Shi, D.N. & Xing, D.Y. Long-range Cooper pair splitter with high entanglement production rate. *Sci. Rep.* 5, 7607; DOI:10.1038/srep07607 (2015).

This work is licensed under a Creative Commons Attribution 4.0 International License. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder in order to reproduce the material. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/