Short-term variability and mass loss in Be stars

III. BRITE and SMEI satellite photometry of 28 Cygni

D. Baade1, A. Pigulski2, Th. Rivinius3, A. C. Carciofi4, D. Panoglou5, M. R. Ghoreyshi6, G. Handler7, R. Kuschnig7,8, A. F. J. Moffat9, H. Pablo10, A. Popowicz10, G. A. Wade11, W. W. Weiss8, and K. Zwintz12

1 European Organisation for Astronomical Research in the Southern Hemisphere (ESO), Karl-Schwarzschild-Str. 2, 85748 Garching b. München, Germany
e-mail: dbaade@eso.org
2 Astronomical Institute, Wrocław University, Kopernika 11, 51-622 Wrocław, Poland
3 European Organisation for Astronomical Research in the Southern Hemisphere (ESO), Casilla 19001, Santiago 19, Chile
4 Instituto de Astronomia, Geofisica e Ciências Atmosféricas, Universidade de São Paulo, Rua do Matão 1226, Cidade Universitária, 05508-900 São Paulo, SP, Brazil
5 Observatório Nacional, Rua General José Cristino 77, São Cristóvão RJ-20921-400, Rio de Janeiro, Brazil
6 Nicolaus Copernicus Astronomical Center, ul. Bartycka 18, 00-716 Warsaw, Poland
7 Institut für Kommunikationsnetze und Satellitenkommunikation, Technical University Graz, Inffeldgasse 12, 8010 Graz, Austria
8 Institute of Astrophysics, University of Vienna, Universitätsring 1, 1010 Vienna, Austria
9 Département de physique et Centre de Recherche en Astrophysique du Québec (CRAQ), Université de Montréal, C.P. 6128, Succ. Centre-Ville, Montréal, Québec, H3C 3J7, Canada
10 Institute of Automatic Control, Silesian University of Technology, Akademicka 16, Gliswice, Poland
11 Department of Physics, Royal Military College of Canada, PO Box 17000, Stn Forces, Kingston, Ontario K7K 7B4, Canada
12 Universität Innsbruck, Institut für Astro- und Teilchenphysik, Technikerstrasse 25, 6020 Innsbruck, Austria

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ABSTRACT

Context. Be stars are important reference laboratories for the investigation of viscous Keplerian discs. In some cases, the disc feeder mechanism involves a combination of non-radial pulsation (NRP) modes.

Aims. We seek to understand whether high-cadence photometry can shed further light on the role of NRP modes in facilitating rotation-supported mass loss.

Methods. The BRITE-Constellation of nanosatellites obtained mmag photometry of 28 Cygni for 11 months in 2014–2016. We added observations with the Solar Mass Ejection Imager (SMEI) in 2003–2010 and 118 Hα line profiles, half of which were from 2016.

Results. For decades, 28 Cyg has exhibited four large-amplitude frequencies: two closely spaced frequencies of spectroscopically significant non-linear. As in η Cen, the ∆ frequency suffers large variations; around maximum the amount of near-circumstellar matter is increased and the amplitude of the Štefl frequency grows by a factor of a few. During such brightenings dozens of transient spikes appear in the frequency spectrum; these spikes are concentrated into three groups. Only 11 frequencies were common to all years of BRITE observations.

Conclusions. Be stars seem to be controlled by several coupled clocks, most of which are not very regular on timescales of weeks to months but function for decades. The combination of g modes to the slow ∆ variability and/or the atmospheric response to it appears significantly non-linear. As in η Cen, the ∆ variability seems to be mainly responsible for the modulation of the star-to-disc mass transfer in 28 Cyg. A hierarchical set of ∆ frequencies may reach the longest known timescales of the Be phenomenon.

Key words. circumstellar matter – stars: emission-line, Be – stars: mass-loss – stars: oscillations – stars: individual: 28 Cygni

1. Introduction

Be stars owe their designation to the occurrence of emission lines forming in a self-ejected Keplerian disc. The latest broad review of the physics of Be stars is available from Rivinius et al. (2013). This so-called Be phenomenon poses two core challenges: a) What enables Be stars to toss up sizeable amounts of mass? Next to rapid rotation (Frémat et al. 2005; Meillard et al. 2012) non-radial pulsations (NRPs) seem to be the most common property known of Be stars (Rivinius et al. 2013, see also their Table 1 for pulsations of individual stars). Following earlier suspicions, long series of echelle spectra of μ Cen finally enabled Rivinius et al. (1998a) to demonstrate that mass-loss events in Be stars can be triggered by the temporary combination of several NRP modes. Paper I in this series (Baade et al. 2016) reported the second such example, based on space photometry of the CDS via anonymous ftp to
cdsarc.u-strasbg.fr (130.79.128.5) or via
table http://cdsarc.u-strasbg.fr/viz-bin/qcat?J/A+A/610/A70

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with BRITE-Constellation. Also in some other Be stars, rotation-assisted multi-mode NRP seems to be a sufficient condition for the occurrence of discrete or repetitive mass-loss events (Baade et al. 2017b,a). Spectroscopically, strictly single-periodic stars such as \(28 \omega\) CMa (Štefl et al. 2003b) with large-amplitude disc variability caution that the condition of multiple modes may not be necessary. But space photometry of \(28 \omega\) CMa conveys a much more complex picture (Baade et al. 2017b). Models for NRP-driven mass loss from rapidly rotating stars (e.g. Ando 1986; Kee et al. 2016b) do not yet take into account strong interactions between a small number of modes. Magnetic toy models are faced with non-detections (Wade et al. 2016).

b) What governs the interface between star and disc? The interplay between mass injection and viscosity rules the life cycle of Be-star discs. The main effect of the viscosity is a redistribution of the specific angular momentum of the ejecta. Only a small fraction of the gas attains Keplerian velocities while the rest falls back to the star. During phases of replenishment, a Keplerian disc can form (Lee et al. 1991). When the supply of new gas is shut off, the inner disc quickly switches from deceleration to accretion. During the further course of time, this transition zone slowly grows and eventually most of the disc becomes an accretion disc (Haubois et al. 2012; Carciofi et al. 2012). The disc is cleared from the inside out as observations also suggest (Rivinius et al. 2001). This somewhat violent coalescence of mass ejection and reaccretion is probably not further complicated by a significant wind of immediate stellar origin (Prinja 1989; Krtiška 2014). Winds in Be stars may obtain a fair part of their supply of matter through radiative ablation of the disc, rather than by accelerating photospheric matter (Rivinius et al. 2013; Kee et al. 2016a).

Near-stellar matter can be approximated as a pseudo-photosphere (Harmannec 1983; Vieira et al. 2015) that re-emits stellar radiation. At optical wavelengths, the region sampled is within very few radii of the stellar photosphere. The observable signature depends on the viewing angle (Haubois et al. 2012) and is largest for near face-on orientations. Circumstellar gas in the line of sight absorbs light (see Fig. 20 for some illustration of the small-angle dependency). Precision photometry can extract much of the information encoded in the short- and mid-term variability of Be stars about both the central star and circumstellar disc. Such photometry requires careful distinction between genuine pulsations and more volatile frequencies that may serve as diagnostics of circumstellar gas dynamics; see Paper I and Rivinius et al. (2016, Paper II). A prominent part of the latter seem to be the so-called (Paper I) Štefl frequencies (Štefl et al. 1998, Sect. 4.5). For unknown reasons they are roughly 10% lower than the dominant spectroscopic frequency.

The relevance of Be stars also has dual, stellar, and circumstellar roots. Be stars combine near-critical rotation with pulsation, making them a test bed of evolution models, and the optical angular diameters of Be discs are among the largest known of viscous (accretion or decretion) discs. For instance, quasar accretion discs measure a few light days across in microlensing events (e.g. Jiménez-Vicente et al. 2012). Active galactic nuclei (AGNs) in Seyfert galaxies are less powerful such that 0.01 pc is an upper limit for them. The most nearby Seyfert galaxies, such as the Circinus Galaxy, NGC 1068, and NGC 4725 are at \(5\)–\(20\) Mpc (Pereira-Santaela et al. 2010), bringing the angular sizes of their AGN to about 0.2 mas.

Most accreting stars in binaries are compact objects with small accretion discs. Only systems with high mass-exchange rates that consist of two main-sequence (MS) stars or an MS star and a giant star develop sizeable discs. Such discs have diameters of no more than a few times that of the MS mass gainers, which typically are cooler and smaller than early-type Be stars. For instance, Zhao et al. (2008) measured the dimensions of the accretion disc of \(\beta\) Lyrae in the \(H\) band as \(1 \times 0.6\) mas. In their Table 2, Rivinius et al. (2013) compiled diameters from optical long-baseline interferometry at various wavelengths of \(22\) Be stars. These stars span approximate ranges of \(0.5\)–\(4\) mas and \(1.5\)–\(15\) stellar radii. In addition to being more extended, Be discs are also very bright. Only the angular sizes of accretion discs around young stellar objects are much larger (by up to \(1\)–\(2\) orders of magnitude; Boley et al. 2013).

These properties permit accretion-disc physics to be studied at high resolution in space, velocity, and time and at an excellent signal-to-noise ratio. For the realization of this diagnostic value, advanced radiative transfer tools have been developed: for example the radiatively driven wind model SMECA (Stee & Bittar 2001, and references therein), HDUST (Carciofi & Bjorkman 2006), and BEDISK (Sigut & Jones 2007). The HDUST model has also been combined with a 1D hydrodynamics grid code (Okazaki 2007) and a 3D smoothed particle hydrodynamics code (Okazaki et al. 2002) to form a viscous decretion disc (VDD) model as employed by, for example Haubois et al. (2012) and Panoglou et al. (2018).

Some of the diagnostically most valuable observations of Be stars are delivered by space-borne photometers. MOST (Walker et al. 2005), CoRoT (Huut et al. 2009; Neiner et al. 2012), and Kepler (Kurtz et al. 2015) have pioneered the field, and the Solar Mass Ejection Imager (SMEI; Jackson et al. 2004; Howard et al. 2013) produced stellar photometry as a byproduct for nearly eight years. For an overview see Rivinius et al. (2017). Currently, BRITE Constellation (Sect. 2.1) is accumulating a large database of naked-eye stars. A first cursory preview of the broad range of variabilities observed by BRITE in Be stars was already published (Baade et al. 2017b,a). Similar to Paper I, the present work uses BRITE space photometry to study the variability of a well-known single object.

\[28 \text{Cyg} = \text{HR} 7708 = \text{HD} 191610 = \text{HIP} 99303\] is a seemingly single B2 IV(e) star (Slettebak 1982) with \(v \sin i = 320\) km s\(^{-1}\) (Rivinius et al. 2003) and no record of shell absorption lines. Rivinius et al. (2006) listed six shell stars between B1 and B3 and an average \(v \sin i\) of \(335\) km s\(^{-1}\) on the Slettebak scale (Slettebak 1982) with a maximum of \(400\) km s\(^{-1}\). For a disc with opening angle \(\leq 20^\circ\), the inclination angle, \(i\), of \(28\) Cyg should, therefore, not exceed \(75^\circ\). Comparison to the sample of Rivinius et al. (2003), which does not include shell stars, suggests a lower limit around \(40^\circ\). The VDD model predicts (Haubois et al. 2012) anti-correlations between colour indices \(U - B\) and \(B - V\) as observed by Pavlovski et al. (1997) in \(28\) Cyg as well as between \(V\) and \(B - V\). A quantitative comparison is impossible because the calculations use a no-disc state for reference, which probably did not occur in \(28\) Cyg, and some maximum state, which the observations cannot be related to. The observed \(U - B\) vs. \(B - V\) slope is compatible with \(30^\circ \leq i \leq 70^\circ\). Haubois et al. (2012) do not illustrate intermediate aspect angles.

\(28\) Cyg was among the first Be stars in which short-term variability was observed (Percy & Lane 1977; Gies & Percy 1977). Spectroscopy followed suit and detected periods near \(0.64\) d (corresponding to a frequency of \(1.56\) c/d; Peters & Penrod 1988; Pavlovski & Ruzic 1990; Hahula & Gies 1994) and \(0.7\) d (corresponding to a frequency of \(1.4\) c/d; Spear et al. 1981; Bossi et al. 1993). Pavlovski et al. (1997) established a photometric peak-to-valley (PTV) amplitude of about \(0.1\) mag in \(V\), and variations in \(B - V\) and \(U - B\) amounted to \(-0.07\) mag.
PTV in both colours without obvious relation to the \( V \) magnitude. From a combination of a subset of these data with other observations, Ružič et al. (1994) inferred frequencies of 1.45 c/d and 0.09 c/d. Percy & Bakos (2001) found it difficult to derive a single-periodic light curve and noted a remarkably low variability of only a few 0.01 mag on a timescale of hundreds of days. The spectroscopic studies presented signatures of non-radial pulsation. The most intriguing are reports by Peters & Penrod (1988) and Peters & Gies (2000) of synchronous variations in photospheric and UV wind lines, i.e. a hypothetical link between pulsations and mass loss (see Sect. 3.3).

From 209 echelle spectra obtained in 1997 and 1998, Tubbesing et al. (2000) confirmed and refined the 1.56 c/d frequency but also deduced a second frequency at 1.60 c/d. Both carried the signature of low-order non-radial \( g \)-mode pulsation that is typical of Be stars (Rivinius et al. 2003). Inspired by the example of \( \mu \) Cen (Rivinius et al. 1998a), the authors searched for indications of enhanced mass loss repeating with the beat frequency of 0.055 c/d. Only one outburst was clearly found to coincide with a moment when both variations reached their maximum amplitude.

2. Observations, data reduction, and analysis methods

2.1. BRIGHT Target Explorer (BRITE)

BRITE-Constellation consists of five nanosatellites as described by Weiss et al. (2014). Pablo et al. (2016) report on pre-launch and in-orbit tests. The pipeline processing from the raw images to the instrumental magnitudes delivered to users is elaborated by Popowicz et al. (2017) who also report per-orbit photometric errors of 2–6 mmag for stars of comparable brightness as 28 Cyg. At \( V = 4.9 \) mag (Ducati 2002), the star is nearly one magnitude brighter than the normal faint end of the capabilities for low-amplitude variabilities with BRITE (Popowicz et al. 2017; Kuschnig, in prep.). After a proprietary period of typically one year, pipeline-processed BRITE data are made public.¹

The datasets for 28 Cyg are summarized in Table 1. BRITE-Constellation members Lem (BLb) and Toronto (BTr) observed 28 Cyg for 15 and 40 d, respectively, in 2014. In a second visit in 2015, Lem and Toronto collected data for 13 and 156 d, respectively, and UniBRITE (UBr) contributed an additional 18 days. The BTr and BLb satellites revisited 28 Cyg in 2016 for another 152 and 18 d, respectively. A \("b\) ("r") in the abbreviation of a satellite refers to the blue 390–460 nm (red 550–700 nm) passband. The observations in 2015 and 2016 were obtained in the so-called chopping mode, in which the satellites nod between two positions slightly farther apart than the width of the PSF. The difference between the on- and off-position aperture photometry is less affected by the progressing radiation damage of the detectors than stare-mode data (Pablo et al. 2016; Popowicz 2016).

The PSF of BRITE varies strongly across the field. Its two nodding positions are enclosed in a window of dimensions 11' × 24' (Popowicz et al. 2017). At any one instant, the PSF covers about one-third of one nodding half of the window. However, pointing and tracking errors introduce considerable exposure-to-exposure jitter, thereby reducing the scope of background removal. For the flux contribution from other discrete sources in the field, see Fig. 3.

¹ URL: http://brite.craq-astro.ca/doku.php

The input data used are from data releases (Popowicz et al. 2017) DR2 for the observations in 2014, DR3 in 2015, and DR5 in 2016. The preparation for time-series analysis (TSA) consisted of detrending the data for dependencies on position (X/Y) and detector temperature. The procedure was the same as in Paper I except that a first very conservative detrending for these three parameters of the data was already applied to the 1-s exposure data. A second such decorrelation was performed with orbit-averaged data mostly with a view towards identifying and eliminating obvious outliers and correcting for any residual trends. For perfect detrending a priori knowledge about the intrinsic variability is required. Because this information does not exist, the data were reduced several times to find the best possible compromise between the removal (mostly by clipping) of artefacts and the preservation of ephemeral events. The detrended signal was applied separately to each so-called set-up (data strings obtained with the same satellite attitude, etc.). Before merging data from various set-ups, small constant offsets were applied if shifts in zero point seemed to require compensation. The (pseudo-)Nyquist frequency of the results is \( f_{\text{orbit}}/2 \approx \frac{12}{2} \) c/d. The resulting light curves are plotted in Fig. 1.

Because BRITE does not perform differential photometry, it is not really possible to determine the intrinsic accuracy beyond the reference values provided by Popowicz et al. (2017). Of course, one could subtract all variabilities found by the TSA and, then, compute some statistics. However, if the purpose is to assess the significance of the frequencies, this and similar methods lead to circular reasoning. As a substitute, Fig. 2 offers the histogram of the magnitude differences between immediately consecutive orbits of BTr in 2015 and 2016, which produced the bulk of the observations (see Table 1). The BTr satellite has an orbital frequency of 14.66 c/d and a duty cycle of 5–27% (Table 1) such that for the observed multiple frequencies of up to 3 c/d (Sect. 3.1.1) the inter-orbit variability is not negligible. Therefore, Fig. 2 only enables a worst-case estimate.

The TSA was performed after conversion of the fluxes to instrumental magnitudes and subtraction of the mean. Three datasets were fully examined, namely the BTr observations from 2015 (Table 2), 2016 (Table 3), and their combination. The much smaller datasets from BLb are noisier and only cover a fraction of the BTr time intervals such that they were omitted from the analysis. Because potentially disturbing low-frequency variability was not seen, no further corrections were attempted.

2.2. Solar Mass Ejection Imager (SMEI)

The SMEI (Jackson et al. 2004; Howard et al. 2013) was a secondary payload on board the Coriolis spacecraft and tasked with monitoring space weather in the inner solar system. The signal recorded for this purpose was the Thomson-scattered solar light from ejected interplanetary electrons. Coriolis was launched in 2003 January into an orbit with a period of 101.6 min. The goal design lifetime was five years, but SMEI was eventually powered off only in 2012 September.

The SMEI delivered nearly \( 4\pi \) surface brightness measurements with three cameras with a field of view of \( 3 \times 120 \) deg² each and a basic angular sampling of 0.2° (0.1° for Camera 3). An inner zone of avoidance of 20° radius enabled some overlap between cameras. Camera 3 observed the region closest to the Sun and Camera 1 observed the zone farthest away from it. Point sources drifted through the combined field of view within ~1.5 min, and continuous 4-s exposures were obtained with one frame-transfer CCD per camera. The core unfiltered photometric passband ranged from 450 nm to 950 nm with a maximum
Fig. 1. Light curve of 28 Cyg observed with BTr (+) and UBr (o) in 2015 (top) and BTr in 2016 (bottom). Fitted constant-amplitude sine curves with frequencies 0.0508 c/d (2015) and 0.0496 c/d (2016) are overplotted in blue and trace the respective \( f_3 - f_2 \). JD = Julian Date. The zero points of the magnitude scales are arbitrary. It should be noted that the difference in magnitude scale between 2015 and 2016. Fifty-seven BeSS spectra were obtained between mJD 632 and 733 (see Figs. 19 and 20).

Table 1. Overview of BRITE observations.

| Satellite name (acronym) | Orbital period [min] | Year | Contig. time [min] | JD start \( -2 450 000 \) | JD end | Range in CCDT [°C] | No. of 1-s exposures | No. of TSA data points |
|-------------------------|---------------------|------|---------------------|--------------------------|--------|---------------------|---------------------|-----------------------|
| BRITE-Lem (BLb)         | 99.7                | 2014 | 7–10                | 6852                     | 6867   | 13.7–22.5           | 3059                | 111                   |
|                         |                     | 2015 | 10–15               | 7274                     | 7287   | 28.7–38.8           | 1781                | 41                    |
|                         |                     | 2016 | 9–14                | 7634                     | 7636   | 25.2–26.6           | 727                 | 20                    |
| BRITE-Toronto (BTr)     | 98.2                | 2014 | 10–16               | 6850                     | 6890   | 7.7–20.3            | 9654                | 251                   |
|                         |                     | 2015 | 5–27                | 7185                     | 7341   | 7.4–22.3            | 105 675             | 2098                  |
|                         |                     | 2016 | 4–27                | 7513                     | 7665   | 7.4–20.4            | 65 454              | 1747                  |
| UniBRITE (UBr)          | 100.4               | 2015 | 7–16                | 7186                     | 7204   | 27.2–29.9           | 7681                | 175                   |

Notes. Suffixes “b” and “r” indicate the passband (blue/red). “Contig. time” denotes the typical contiguous time interval per orbit during which exposures were made. CCDT is the temperature of the detector. The BTr observations after JD 2 456 877 suffered from excess noise and reduced instrumental throughput and were discarded.

near 700 nm. After an electronics failure in 2006, the temperature of Camera 3 rose, and its performance gradually degraded substantially.

The PSF of the deliberately defocussed cameras measures \( \sim 1° \) across, is highly asymmetric, and varies strongly over the path along which an object moved through the field of view (Hick et al. 2007). With its aperture of 1.76 cm\(^2\), SMEI could detect point sources of \( \sim 10^8\). Surface-brightness measurements with a precision of 0.1% required careful removal of stars brighter than \( \sim 6^\circ \) from the images (Hick et al. 2007). In addition to direct and scattered light from discrete solar-system objects, the strongest background signal by far was the zodiacal light, which in some directions exceeded the signal from solar mass ejections by two orders of magnitude. It was removed by careful modelling. However, apart from any systematic issues, the stellar SMEI data inherited much photon noise from this background, to which the South Atlantic Anomaly made additional contributions. Radiation damage of the CCDs caused a loss in sensitivity of 1.6% per year and cosmetic problems.

Stellar fluxes (in SMEI magnitudes; Buffington et al. 2007) extracted by the UCSD pipeline (Hick et al. 2005) are available.
Fig. 2. Histogram of the magnitude differences between directly consecutive orbits (data points) of BRITE satellite BTr in 2015 (dotted line) and 2016 (solid line).

Table 2. BRITE photometry of 28 Cyg with satellite BTr in 2015.

| HJD − 2 457 000 [d] | Flux [mag] |
|----------------------|------------|
| 184.6737             | +0.007     |
| 184.7420             | −0.009     |
| 184.8098             | −0.023     |
| 184.8782             | −0.016     |
| 184.9476             | −0.010     |

Notes. The zeropoint of the BRITE magnitude scale is arbitrary (complete table available from CDS).

Table 3. BRITE photometry of 28 Cyg with satellite BTr in 2016.

| HJD − 2 457 000 [d] | Flux [mag] |
|----------------------|------------|
| 512.9362             | −0.024     |
| 513.0040             | −0.002     |
| 513.0726             | −0.001     |
| 513.1407             | +0.001     |
| 513.2089             | −0.010     |

Notes. The zeropoint of the BRITE magnitude scale is arbitrary (complete table available from CDS).

The only accompanying telemetry are observing dates and times so that it is not possible to analyse the observations separately for each camera. This has major repercussions as demonstrated below. So many years after the termination of the SMEI mission, the contact address provided at the UCSD SMEI Web site seems no longer actively supported. An example of observations with SMEI of relatively faint objects (novae) is available from Hounsell et al. (2010) who provide overall absolute errors around maximum (3.5–5.4 mag) of 0.01–0.02 mag.

The SIMBAD (Wenger et al. 2000) database lists 443 sources within 0.6° from 28 Cyg. Only relatively few have magnitudes in the R band, which is the best match of the sensitivity of SMEI. B and V fluxes for 323 and 314 sources, respectively, in SIMBAD account for 1.2 and 2.2 times as much flux as 28 Cyg alone. The distribution of these fluxes in annuli of 3 arcmin width is shown in Fig. 3.

The SMEI observations of 28 Cyg extended over 7.9 yr from February 4, 2003 to December 30, 2010 such that the nominal frequency resolution is ≤0.001 c/d. This dataset comprises a total of 34 335 data points. Since each data point results from one orbit, more than 80% of all orbits contributed, and the nominal Nyquist frequency is ∼7.1 c/d. After removal of extreme outliers, the raw light curve (Fig. 4) revealed a strong need for correction for instrumental annual and other long-term variability. In addition, at some phases, the distribution of data points is bimodal, which is possibly due to the combination of data from different cameras. After pre-whitening for the annual variability by subtracting means in phase intervals of 0.01, a considerable annual pattern was still left because of season-dependent excess noise. These annual phase intervals were removed from the dataset, which thereby shrunk to 26 157 data points. Another 1184 presumed outliers were eliminated after its inspection.

Next, the spacing in time of the remaining 24 973 observations was studied. It can vary if the posted times correspond to the mean time of the 4-s exposures co-added for each orbit and the number of the latter varies because of rejected exposures. It was hypothesized that the best orbital data points are those that result from orbits without rejected measurements and that they can be identified by their spacing corresponding closely to the orbital period of 101.6 min. This selection reduced the number

2 http://smei.ucsd.edu/new_smei/data&images/stars/timeseries.html
Fig. 5. SMEI light curve of 28 Cyg after subtraction of the instrumental annual variation shown in Fig. 4 and after elimination of data from annual phases with elevated noise. In addition, some extreme outliers are clipped in this figure. No indication is visible of any photometric equivalent of the fading of the Hα emission between 2005/2007 and 2013 (Sect. 3.3). Overplotted in blue is a fitted sine curve with frequency 0.00471 c/d.

Table 4. SMEI photometry of 28 Cyg with satellite BTr in 2016.

| HJD − 2457000 | Flux |
|----------------|------|
| 2675.4621      | −0.050 |
| 2675.5327      | −0.031 |
| 2676.5208      | +0.049 |
| 2676.5913      | +0.055 |
| 2676.6619      | +0.133 |

Notes. The zeropoint of the SMEI magnitude scale is arbitrary (complete table available from CDS).

of data points to 23 708. Before this scheme was adopted, various others were explored, including permutations of the above steps. When the filtering according to the time elapsed between consecutive data points was performed at the beginning, it eliminated far more measurements than when done at the end. This demonstrates that the filtering of the annual light curve, which contains some subjective elements, has an objective background.

In addition to the annual variability (Fig. 4), SMEI data suffer instrumental variabilities faster than a year but slower than those measured in the BRITE observations of 28 Cyg (Sect. 3.1 and Table 5). Figure 5 depicts the full light curve with all corrections applied as described above. For the observations with SMEI of α Eri (B6 Ve), ζ Pup, and ζ Oph (O9.5 V), Goss et al. (2011), Howarth & Stevens (2014), and Howarth et al. (2014), respectively, used a boxcar filter of width 10 d to remove spurious non-stellar signals. In spite of the low accuracy of the individual SMEI measurements, their large number and long time span permitted these studies to detect significant variabilities at frequencies 0.7−7.2 c/d with amplitudes down to a few mmag. Experiments with filter widths between 6 d and 15 d showed that in the range above 0.5 c/d, where most of the BRITE frequencies occur, the results of the TSA are not very sensitive to the choice of the filter width, and it was decided to not apply any such filtering. The frequencies in common with both BRITE observing runs and their amplitudes are included in Table 5. All values therein are averages over the full range in time.

Figure 5 indicates the presence of some very slow regular variability. In the frequency spectrum, there is a strong, well-isolated peak at \( f_T = 0.00471 \) c/d. The associated semi-amplitude is 16.7 mmag, i.e. far higher than any of the variations seen with BRITE. A sine fit with this frequency is overplotted in Fig. 5. Between phases 0.7 and 1.0, a similar bi-modal distribution of values as in the annual light curve (Fig. 4) is seen. The variability may, therefore, be due to an imperfect relative calibration of the cameras. For comparison, the SMEI data of some stars with similar positions in the sky (λ Cyg [B5 V], ν Cyg [B2 Vne], QR Vul [B3 Ve]) were analysed. Very strong variability with 0.00411 c/d was found in ν Cyg and in QR Vul with 0.00473 c/d. Accordingly, \( f_T = 0.00471 \) c/d is not thought to be intrinsic to 28 Cyg.

The statistical properties of the SMEI data at their high-frequency end are illustrated by Fig. 6 which presents a histogram of the magnitude differences between directly consecutive orbits (data points) of the SMEI data shown in Fig. 5.

Fig. 6. Histogram of the magnitude differences between directly consecutive orbits (data points) of the SMEI data shown in Fig. 5.
Table 5. Mean seasonal values of frequencies and semi-amplitudes in 28 Cyg.

| Frequ. ID | BTr 2015 | BTr 2016 | BTr2014-2016 | SMEI | Hørs |
|-----------|----------|----------|---------------|------|------|
|           | Freq. [c/d] | Amplit. [mmag] | Freq. [c/d] | Amplit. [mmag] | Freq. [c/d] | Amplit. [mmag] | Freq. [c/d] | Amplit. [mmag] | Freq. [c/d] |
| \(f_{322}, f_{\Delta b}\) | 0.0508 | 8.5 | 0.0496 | 12.8 | 0.0517 | 9.6 | 0.05093 | 2.3 |
| 1.3164 | 3.3 | 1.3177 | 5.4 | 1.3180 | 3.8 |
| 1.3603 | 2.2 | 1.3605 | 5.0 | 1.3599 | 3.0 |
| 1.3713 | 3.2 | 1.3691 | 4.2 | 1.3693 | 3.7 | 1.36809 | 2.3 |
| \(f_{1}, f_{a}\) | 1.3799 | 6.8 | 1.3800 | 8.5 | 1.3811 | 6.6 | 1.37992 | 5.1 |
| \(f_{2}, f_{b}\) | 1.5448 | 5.4 | 1.5446 | 5.5 | 1.5452 | 5.2 | 1.54470 | 3.3 | 1.54562 |
| \(f_{3}, f_{c}\) | 1.5977 | 5.3 | 1.5976 | 6.5 | 1.5973 | 5.9 | 1.59695 | 1.3 | 1.59726 |
| 2.6769 | 3.9 | 2.6768 | 5.7 | 2.6761 | 4.5 |
| 2.7326 | 2.6 | 2.7319 | 4.4 | 2.7323 | 3.0 |
| 2.7407 | 2.5 | 2.7423 | 3.1 | 2.7420 | 2.5 | 2.74294 | 1.0 |
| \(\approx f_2 + f_3\) | 3.1425 | 1.9 | 3.1427 | 1.9 | 3.1425 | 1.5 |

Notes. The list only contains frequencies detected with BRITE in both 2015 and 2016 that agree to within 0.002 c/d.

Fig. 7. BRITE frequency spectrum (in arbitrary units) of 28 Cyg. *Top:* frequency spectrum from 2015 for BTr and UBr satellites is shown; *bottom:* frequency spectrum from 2016 for BTr satellite is shown. Arrows denote the frequencies included in Table 5. The dashed lines represent the local sum of mean power and the × the scatter calculated after removal of the frequencies in Table 5. Between 3.5 c/d and the nominal Nyquist frequency near 7.2 c/d, there is virtually no power. Frequency groupings occur at the approximate ranges 0.1–0.5 c/d (\(g_0\)), 1.0–1.7 c/d (\(g_1\)), and 2.2–3.0 c/d (\(g_2\)).

3. Analysis results

3.1. BRITE

3.1.1. Common periodic variations in 2015 and 2016

Figure 7 presents the frequency spectra of the BTr observations in 2015 and 2016 (Fig. 1). Beyond 3.5 c/d, no significant features can be found above the general noise floor. Obvious evidence for 1 c/d and related peaks cannot be seen either. A global pictorial overview of the variability of 28 Cyg as observed by BRITE is provided by the two time-frequency diagrams in Fig. 8.

In the BRITE frequency spectra, the three highest peaks above 0.5 c/d occur at \(f_1 = 1.381\) c/d, \(f_2 = 1.545\) c/d, and \(f_3 = 1.597\) c/d (here and in the following, all frequencies, etc. are from the combined analysis of the BTr observations in 2014, 2015, and 2016 unless explicitly identified otherwise). The strongest peak below 0.5 c/d appears at \(f_{322} = 0.052\) c/d. This slower
Fig. 8. Time vs. frequency diagrams for the BRITE red-filter photometry of 28 Cyg in 2014. The bottom panel shows a single time bin, the middle panel shows 2015, and the top panel represents 2016. The discrete Fourier transform frequency spectra were calculated in 40-day intervals with a step of 1 d. The common amplitude scale appears on the right. Horizontal lines occur where data from different set-ups were stitched together. It should be noted that the diffuse appearance of $f_{\Delta 32}$ (0.05 c/d) and $f_{1}$ (1.38 c/d, the Štefl frequency) and the cyclic anti-phased variability of the two $g$ modes $f_{2}$ (1.54 c/d) and $f_{3}$ (1.60 c/d).

Fig. 9. Light curve from BTr 2015 from Fig. 1 binned to steps of 0.02 in phase of the 0.0508-c/d frequency ($f_{\Delta 32}$). Zero points of flux and phase are arbitrary. For the same bins, the crosses indicate the scatter of the 2015 magnitudes in Fig. 1. It should be noted that the sign of the magnitude scale; the scatter is largest during light maxima.

In 2015, 28 Cyg did not undergo any obvious outburst signalling mass loss (Fig. 1). However, Fig. 9 suggests small enhancements of the photometric scatter during the maxima of the variability with $f_{\Delta 32}$. The phase dependency of the scatter became very visible (Fig. 10) in 2016. The main contribution to this was made by the last three $f_{\Delta 32}$ cycles in 2016, the amplitudes of which were up to an order of magnitude higher than in the five preceding cycles (Fig. 1). At the time of these brightenings, the light curve also exhibited interspersed short fades well below the mean flux level.

Between the above frequencies, the following relation exists:

$$0.0517 \text{ c/d} = f_{\Delta 32} \approx f_{3} - f_{2} = 0.0521 \text{ c/d}.$$ 

The deviation from full equality amounts to 0.0004 c/d, which is of the order of the nominal single-season errors. Figure 1 presents the light curve associated with $f_{\Delta 32}$ in 2015 and 2016.
before the strong increase in amplitude of the $f_{32}$ variability around mJD = 610 (Fig. 1; mJD denotes a modified Julian Date: HJD – 2 457 000). However, during that phase of increased overall photometric amplitude, the amplitude of $f_1$ displayed semi-regular large-amplitude variations with a cycle length comparable to, but clearly different from, that of $f_{32}$ (Fig. 13). There was similar activity at the end of the observations in 2015 (Fig. 13). By contrast, the amplitude variations of $f_2$ and $f_3$ (Fig. 13) were an order of magnitude lower than those of $f_1$. The difference between the stellar variabilities with $f_2$ and $f_1$ and the exospheric variability with $f_1$ is very well visible in Fig. 8.

3.1.2. Ephemeral variations

Figure 7 gives rise to the suspicion that ephemeral elements form a major part of the variability of 28 Cyg. Motivated by the strong changes around mJD 600, the 2016 data were split into two sets: mJD $\leq$ 600 and mJD $>$ 600. The differences between their frequency spectra are stunning (Fig. 14). The extra features during the outburst may be mixtures of (i) combination frequencies; (ii) harmonics; (iii) side lobes due to the large-amplitude variations of $f_{32}$; (iv) circumstellar variations; and/or (v) stellar pulsations. Since none of these was detected in two or more independent datasets, their large number makes it next to impossible to identify the nature of any such single feature and their short lifespans prevent their characterization as periodic.

Temporarily enhanced visibility is not necessarily the same as increased amplitude or power. In very rapidly rotating stars, the angular parts of NRP eigenfunctions are described by a series of spherical harmonics (Lovekin & Deupree 2008). If the decomposition of eigenmodes into spherical harmonics changes during an outburst or brightening, this could also modify their visibility. In that case, such modes would not add to the cause of outbursts or brightenings. At the current level of analysis, only $f_{32}$ can be considered as causing mass loss.

The variability of Be stars is not erratic or even chaotic: the clear signature of low-order $g$-mode pulsations in high-resolution spectra (Rivinius et al. 2003) demonstrates coherent, and coherently varying, large-scale structures in the photosphere. Moreover, for several dozen spikes in the frequency spectrum the data were convolved with the corresponding

Fig. 11. Variability of $f_2$ and $f_3$ in 2015 (top) and 2016 (bottom). Frequencies were measured in a window of 40 d stepped by 1 d. The overplotted blue dotted lines are fitted sine curves with frequency 0.0508 c/d (2015) and 0.0496 c/d (2016), tracing the respective mean $f_{32}$.

Fig. 12. Variability of $f_3$ in 2015 (top) and 2016 (bottom). Frequencies were measured in a window of 40 d stepped by 1 d.

The large number of temporary frequencies prompted a search for frequency variations of $f_1$, $f_2$, $f_3$, and other frequencies in single-season data. For each frequency, a sine curve was fitted to 40-d intervals of the dataset concerned, and this time window was shifted in steps of 1 d. No frequency appeared constant (Fig. 8). However, lower amplitude frequencies exhibited higher scatter, and the shorter time interval of 40 d implies larger uncertainties in general. Except for $f_1$ to $f_3$, which are discussed in the following, the results are, therefore, mostly inconclusive.

In both 2015 and 2016, $f_2$ and $f_3$ were modulated with their $\Delta$ frequency, $f_{32}$. The semi-amplitudes amounted to 0.005–0.007 c/d and $f_2$ and $f_3$ occurred nearly in anti-phase (Figs. 8 and 11). There is no signature of the large increase in amplitude of $f_{32}$ in the last two months of the 2016 observations. To test the robustness of the result, the time interval was varied between 20 d and 60 d in steps of 5 d. There was no elementary change, and the anti-phased modulation of $f_2$ and $f_3$ was confirmed in all cases. But the amplitude was much reduced at 60 d and $f_3$ and $f_2$ were no longer properly resolved towards 20 d because, in that case, the length of the interval corresponds to 1/(3f_1 – 2f_2).

A similar frequency modulation does not affect the nearby $f_1$. The $f_1$ frequency only suffered a major perturbation (Fig. 12)
Fig. 14. Frequency spectra of the red 2016 BRITE observations before (top) and after (bottom) mJD 600 when a series of brightenings began (see Fig. 1). Power is given in arbitrary units. The arrows have the same meaning as in Fig. 7, and the full-season error curve (arbitrarily scaled) from Fig. 7 is also shown. In the top panel, frequency groups $g_1$ (1.0–1.7 c/d) and $g_2$ (2.2–3.0 c/d) are well separated.

Fig. 15. Frequency spectrum (in arbitrary units) of the SMEI data in the region of the main BRITE frequencies above 0.5 c/d ($f_a$: 1.381 c/d, $f_b$: 1.545 c/d, and $f_c$: 1.597 c/d). Frequencies, and in most cases the resulting light curve had an approximately sinusoidal shape.

Finally, the frequency spectra of the 2015/16 BTr data were searched for patterns by calculating histograms of nearest neighbour differences, frequency spectra (of the frequency spectra), and cross-correlation functions. The results were all negative, except for a possible overabundance of differences close to 0.01 c/d (e.g. 1.369 c/d – 1.360 c/d and 2.742 c/d – 2.732 c/d in Table 5; 1.369 and 2.742 c/d are harmonics). In the SMEI frequency spectrum, a feature exists at 0.00995 c/d; at 8.6 mmag, the amplitude is large. A similar light curve arises from the BTr observations in 2016.

3.2. Solar Mass Ejection Imager

The three main BRITE frequencies above 0.5 c/d also stand out in the SMEI data (Fig. 15). Peaks at $f_a = 1.3799$ c/d, $f_b = 1.5447$ c/d, and $f_c = 1.5970$ c/d can be identified with $f_1$, $f_2$, and $f_3$ (Table 5). That is, the mean frequencies in 2003–2010 (SMEI) and in 2014–2016 (BRITE) were the same. The long duration of the SMEI observations permits the constancy of the frequencies to be examined on shorter timescales. The results of single sine curves fitted to the data (Fig. 16: amplitudes; Fig. 17: frequencies) exhibit some commonalities of the amplitude variations of $f_2$ and $f_3$ whereas the behaviour of $f_1$ is different and more pronounced. With a factor of ~3, the largest relative amplitude variation was associated with $f_{\Delta 32}$.

In the SMEI observations, a similar relation exists between $f_{\Delta}$, $f_b$, and $f_c$ as between $f_1$, $f_2$, and $f_3$ with BRITE, i.e.

$$0.05093 \text{ c/d} = f_{\Delta/32} \approx f_c - f_b = 0.05225 \text{ c/d}.$$  

The light curve after pre-whitening for 0.00471 c/d (Sect. 2.2) suggests that SMEI did not capture outbursts larger than 0.05 mag and longer than 100 d. This is in agreement with, but less stringent than, the BRITE observations (Sect. 3.1) and the findings of Percy & Bakos (2001). Even after this correction, no hint of a photometric counterpart of the fading of the H$\alpha$ emission from 2005/2007 to 2013 (Sect. 3.3) is present.
3.3. Spectroscopy

Tubbesing et al. (2000; see also Sect. 1) found two frequencies, \( f_1 = 1.54562 \text{ c/d} \) and \( f_2 = 1.60033 \text{ c/d} \) with radial velocity amplitudes of \( \sim 20 \) and \( \sim 10 \text{ km s}^{-1} \), respectively. If corrected for a likely 1-c/yr alias, \( v_2 \) becomes 1.59726 c/d, and \( v_1 \) and \( v_2 \) can be perfectly identified with BRITE frequencies \( f_2 = 1.5453 \text{ c/d} \) and \( f_3 = 1.5973 \text{ c/d} \), respectively. The associated line profile variability seems to be of the same \( \ell = \pi - \nu = 2 \) \( g \)-mode variety that is typical of classical Be stars (Rivinius et al. 2003). Accordingly, \( f_2 \) and \( f_3 \) are due to non-radial pulsation \( g \)-modes.

As of February 2017, the BeSS database (Neiner et al. 2011) contained 118 wavelength-calibrated H\( \alpha \) line profiles contributed by more than a dozen amateurs between 1995 July and 2017 January; about half of these line profiles were contributed in 2016. Those observed since August 1997 were downloaded from the BeSS Web site. The equivalent widths derived from the line profiles are presented in Fig. 18. Like the photometry, the contemporaneous H\( \alpha \) spectroscopy conveys the picture of 28 Cyg as one of the more quiet early-type Be stars. The H\( \alpha \) line emission was at a crudely constant high level through the end of 2002. From mid-2007 until early 2012 the H\( \alpha \) line emission was weak but again fairly constant. Thereafter, the line emission started to rise but did not reach the previous high level. The BRITE photometry started nearly three years after the onset of this partial recovery. During the BRITE observations the line emission stayed at some plateau with little variability. The overall timescale is at the long end of such cycles (e.g. Ghoreyshi et al. 2016).

There are no BeSS spectra from 1998 when Tubbesing et al. (2000) observed an outburst with H\( \alpha \). A single H\( \alpha \) profile 20 d before the amplitude maxima of \( f_1 \), \( f_2 \), and \( f_3 \) seen by SMEI (Sect. 3.2) is free of anomalies. Of the 62 BeSS spectra from 2016, 57 were obtained between mJD 630 and 740 in response to an alert when the online control of the BRITE observations had recognized the increased activity starting around mJD 600. The spectra were manually normalized with fitted splines, resampled from their original wavelength bins between 0.03 A and 0.18 A to a common 0.1 A, and are plotted in Fig. 19.

The two H\( \alpha \) emission peaks are well, albeit not perfectly, approximated by Gaussians so that differential measurements from fitted Gaussians make sense. Figure 20 presents the variability in total equivalent width, peak-height \( (V/R) \) ratio, and peak separation measured in the BeSS spectra; because of the inhomogeneous provenience of the observations only rough error estimates can be given. After mJD 650, there was a gentle increase by 25% in equivalent width. At about the same time, a fairly marked drop by more than 10% occurred in the peak separation. No attempt was made to search for repetitive variability on any timescale.

From 44 ground-based spectra Peters & Penrod (1988) derived an NRP period of 16.5 h (f: 1.45 c/d), which is a blend of \( f_1 - f_3 \), and found it co-phased with the equivalent width of CIV \( \lambda \lambda 1548, 1551 \) in 17 R \( \approx 10,000 \) spectra from the International Ultraviolet Explorer (IUE; Boggess et al. 1978). In 25 IUE spectra obtained within 56 h, Peters & Gies (2000) found a period of 0.646 \( \pm \) 0.019 d (1.55 \( \pm \) 0.05 c/d; i.e. very close to \( f_2 = 1.545 \text{ c/d} \) and still consistent with \( f_3 = 1.600 \text{ c/d} \)). Because
the flux amplitude increased towards lower wavelengths, it was attributed to pulsational temperature variations. The C IV λ 1551 wind line exhibited correlated variability in equivalent width while the photospheric C III λ 124.7 nm and Si II λ 126.5 nm lines did not. However, Peters & Gies did not state whether the variability in line strength was above the escape velocity so that the relation to genuine mass loss is not clear.

3.4. Caveats and numerical limits

The analysis of the photometry of 28 Cyg reaches a fundamental mathematical limit: to measure a frequency \( f \), a conservative rule of thumb is that the data should cover a time interval \( T \geq 2/f \). In the presence of noise, intervals larger by an order of magnitude are desirable. If the case of closely spaced power peaks, which, moreover, undergo independent variations, this minimal duration does often not suffice. The timescales of frequency and amplitude variations in 28 Cyg are comparable to this safe width of time windows. This touches upon the definition of a frequency.

Figure 8 illustrates the complexity of the variabilities, their variations in both frequency and power, in a single picture. For the numerous secondary frequencies (Sect. 3.1.2), error, and significance analyses attain a very limited meaning in the presence of the numerous interrelations.

The remainder of the paper only discusses frequencies \( f_1 \), \( f_2 \), \( f_3 \), and \( f_{32} \) (Table 5), all four of which were detected by BRITE in 2015 and 2016 (Sect. 3.1) and were confirmed with SMEI (Sect. 3.2). Moreover, \( f_2 \) and \( f_1 \) were spectroscopically discovered first. The maximal differences between the photometric values of these four frequencies are 0.0001, 0.0002, 0.0007, and 0.0013 c/d, respectively. Figure 8 suggests a frequency jitter above that level. Therefore, Table 5 only contains frequencies detected in both BRITE datasets (from 2015 and 2016) and those agreeing to better than \( \sim 0.002 \) c/d. As becomes amply clear below, only very few of the many processes in 28 Cyg, if any, seem to be running on clocks with that precision. Moreover, the entries in Table 5 are seasonal averages. There are only 11 such seemingly persistent frequencies; these frequencies are indicated in Fig. 7.

A low-threshold search between 0 and 3.5 c/d at a sampling of 0.001 c/d found \( \geq 60 \) frequency peaks in 2015 and \( \geq 100 \) in 2016. For randomly distributed frequencies, the probability of chance coincidences within 0.002 c/d is, in that case, less than 6%. It is lower for the much fewer high-amplitude variabilities of Table 5. For a set of n lines in two independent observations (BRITE and SMEI), the single-frequency probability is raised to the nth power. The dashed lines in Fig. 7 indicate 3σ noise levels after subtraction of these variabilities. This rigorous approach does not take into account the large-amplitude variability of \( f_{32} \), especially at the end of the observations from 2016 (Fig. 1). Moreover, this approach attributes all other variability completely to stellar or instrumental noise. Such a classification system may be too crude for the variability of 28 Cyg (Sect. 3.1.2).

For reference, Kallinger et al. (2017) determined a total of 22 frequencies with errors between 0.9 and 92 \( \times 10^{-5} \) c/d and amplitudes from 0.6 to 17 mmag from BRITE observations of the SBP star HD 201433. The SMEI and BRITE frequencies agreed at the 0.8 and 1.8σ level, respectively. In the longer SMEI observing sequences, nine rotationally split frequency pairs could be resolved.

Given the large PSFs of SMEI and BRITE, there is the risk that the main frequencies \( f_1 \), \( f_2 \), \( f_3 \), and \( f_{32} \) are not intrinsic to 28 Cyg but are contributed by one or more other stars. Any such star would need to have fallen into the apertures of both SMEI and BRITE. The radius of a circle including the PSF at both nodding positions is \( \sim 12 \) arcmin. As of August 2017, the International Variable Star Index (Watson 2006) in VizieR (Ochsenbein et al. 2000) contains two variable stars within 15 arcmin from 28 Cyg. One (VSX J200906.4+365552) is an M5 V star that is listed as varying in \( R \) between 8.4 and 8.8 mag with unknown period. No period is known for the other star (VSX J201000.6+365111) as well and the stated \( R \) magnitude range is 11.8–12.4 mag.

In principle, this still leaves dozens of other objects as hypothetical real sources of the observed frequencies. However, since \( f_{32} \) is the difference between \( f_3 \) and \( f_2 \), these three frequencies must be from one and the same star. Moreover, \( f_3 \) and \( f_2 \) were detected spectroscopically so that the common source of these three frequencies was in the aperture of the spectrograph. Only \( f_1 \) could be from a second star; however, there are plausible reasons (Sect. 4.3) to identify it as the Štefl frequency of this Be star.

4. Discussion

4.1. Conceptual framework

Most Be stars undergo large-scale variations of their discs on timescales of years. Changes in total disc mass manifest themselves in varying H\( \alpha \) emission-line strengths and photometric amplitudes of several 0.1 mag (e.g. Keller et al. 2002). Evidence of more nearly periodic slow photometric variability in Be stars is still restricted to shorter timescales. Labadie-Bartz et al. (2017) present light curves of 11 Be stars with apparent periods \( >80 \) d. However, it is impossible to recognize any Be star by specific properties of this variability. Perhaps, this informational shallowness is the reason why the key to the understanding of the Be phenomenon has not been found therein.

Superimposed on this slow variability are outbursts. Their spectroscopic record is particularly rich and multifaceted for \( \mu \) Cen, reaching from pulsationally triggered mass ejections (Rivinius et al. 1999a) via new matter settling in the circumstellar disc (Baade et al. 1988; Hanuschik et al. 1991) to gas moving towards the star at high velocity (Peters 1986; Neiner et al. 2002) also captured an outburst in spectra of \( \omega \) Ori.

The build-up of line emission, i.e. a disc, as well as super-equatorial velocities associated with Štefl frequencies (Štefl et al. 1999) are evidence of star-disc mass transfer. There may also be numerous failed mass-loss events, during which matter is tossed up but does not reach an orbit as suggested by rapid variability in broadband polarimetry (Carciofi et al. 2007). Such cases are not easily diagnosed by spectroscopy but may still emit additional light or remove light from the line of sight, or both. Therefore, in the following we discuss brightenings and leave open from which level on they may be photometric equivalents of spectroscopic mass-loss events. Inspection of the light curve (Fig. 1) shows that 28 Cyg fairly regularly experiences brightenings with amplitudes well above the higher frequency variability floor.

For the interpretation of apparent exophotospheric photometric variability, the model calculations by Haubois et al. (2012) are used as the foundation. These models imply that at an inclination angle near 70° the photometric variability due to emission from variable amounts of near-stellar matter vanishes. On this basis, estimates of the inclination angle of 28 Cyg, 40° < \( i \) < 75° (Sect. 1), suggest that matter ejected into the equatorial plane produces extra emission that ought to reveal itself as brightenings (see also Fig. 21, top panel). However,
the sensitivity may be small. In the wavelength region covered by BRITE Constellation, the matter involved is expected within about two radii of (one radius above) the stellar photosphere (Haubois et al. 2012). Photometry alone cannot determine whether this matter is already part of the disc, drifting towards it, or falling back to the star. It may form one large contiguous structure or be fractionated into numerous small blobs. Therefore, in the following we use the term exospherically modulated spectra to allude to such situations.

The aspect-angle dependence may be different if matter were also lost at higher stellar latitudes (as also considered by Štefl et al. 2003a; Wisniewski et al. 2010). The ejecta may initially subtend an angle comparable to or smaller than the photosphere so that they absorb photospheric radiation as they quickly cool radiatively below the photospheric temperature. With time, the material spreads out, becomes much less dense, and partly enters the atmosphere to this slow and possibly non-adiabatic variability.

4.2. Slow and irregular variability

The clearest indicator of structural variations of Be discs is the violet-to-red ratio of emission peaks, \( V/R \). It is a robust estimator as it only requires a differential measurement. In high-inclination stars such as 28 Cyg, the large rotational peak separation makes \( V/R \) variations easily detectable. This peak separation can be induced on very different timescales as global disc oscillations by the quadrupole moment of a rotationally distorted central star (Okazaki 1997), dynamically by any sufficiently massive and close companion (Štefl et al. 2007; Panoglou et al. 2018), radiatively by a hot companion (e.g. Peters et al. 2013; Mourard et al. 2015), and by non-axisymmetric mass injections. Also in this respect, 28 Cyg is at the far quiet end of the activity scale of early-type Be stars.

The persistent high degree of symmetry of the \( \text{H}\alpha \) line emission suggests that any undetected companion star is too ineffective in affecting the disc. Therefore, the explanation of the slow equivalent-width variations of the \( \text{H}\alpha \) profiles (Fig. 18), which leave no doubt that the disc around 28 Cyg was eroded for some years and was replenished around 2013, must be sought in a single-star context. Contrary to many years of ground-based photometric monitoring, Tubbing et al. (2000) recorded a discrete mass-loss event in 1998, when the absolute value of the \( \text{H}\alpha \) equivalent width dropped by \( \sim 30\% \). The event lasted 10–15 d and was the only one observed in two seasons. The low level of disc activity is confirmed by the five-months BeSS snapshot (Figs. 19 and 20), during which no such event was observed (i.e. after the brightening starting around mJD 600). The slow variability is probably due to oscillatory disc instabilities (Okazaki 1997).

The low variability in line emission is noteworthy because in the VDD model, without replenishment, Be discs are re-accreted within months to years (Carciofi et al. 2012; Vieira et al. 2017). Radiative ablation may accelerate this process (Kee et al. 2016a). Therefore, one might expect the \( \text{H}\alpha \) line emission to be fairly variable. The simplest resolution of this puzzle may consist of quasi-continuous star-to-disc mass transfer, which could also include small outbursts every couple of weeks.

4.3. The \( g \) modes \( f_2 \) and \( f_3 \) and other stellar variabilities

The most remarkable fact about the variability of 28 Cyg is the tight link, via \( f_{32} \), between the two \( g \) modes with \( f_2 \) and \( f_3 \). Neither the reason nor the geometric depth of the combination is known. It could be just a linear superposition and merely appear as a coupling due to the extra emission from the mass ejection; it could be amplified by a non-linear response of the atmosphere to this slow and possibly non-adiabatic variability. There could also be non-linear mode coupling deep inside the star (Dziembowski 1978).

Two closely spaced frequencies also form part of an anchor variability pattern (cf. Sect. 4.1) in many other (early-type) Be stars. Examples include \( \eta \text{Cen} \) (Paper I), \( \psi \) Per, 25 \( \phi^1 \) Ori (Baade et al. 2017a), 10 CMa, and 27 CMa (Baade et al. 2017b). However, in pole-on stars, the light curves are dominated by emission from varying amounts of near-stellar matter that blankets any underlying stellar variability. \( \mu \text{Cen} \) (Paper I), \( \kappa \) CMa, and \( \omega \) CMa (Baade et al. 2017b) are such cases. Therefore, the fraction of (early-type) Be stars with observed photometric \( \Delta \) frequencies is always lower than the genuine incidence of \( \Delta \) frequencies. If many Be stars exhibit large-amplitude \( \Delta \) frequencies, the conditions for their formation should not be too special.

Among the frequencies investigated, \( f_2 \) and \( f_3 \) are the most stable (Figs. 8, 11, and 17; Table 5). However, these frequencies undergo a subtle modulation with \( f_{32} \), i.e. their own difference. Not any less mysterious is that \( f_2 \) and \( f_3 \) vary in anti-phase (Figs. 8 and 11). This may harbour some hint as to how and where the coupling of these two NRP modes takes place. While it is still conceivable that the \( \Delta \) frequency modulates the position of the layer where the waves associated with the \( g \) modes are reflected and thereby modulates their apparent frequencies, it is not at all clear why two very closely spaced frequencies are affected in anti-phase.

Also the constancy in amplitude of \( f_2 \) and \( f_3 \) stands out above much of the rest (Figs. 8, 13, and 16). If the mass-loss modulation and apparent driving with \( f_{32} \) (Sect. 4.4) were ultimately powered by these two \( g \) modes, one might not expect this. Comparison to ground-based studies shows that most of them found some blend of \( f_1 \), \( f_2 \), and \( f_3 \) but could not resolve it. The implied apparent variability of the frequencies contributed to the notion
prevailing at that time that the rapid variability of Be stars is mostly semi-regular. Thanks to BRITE and SMEI it is now clear that stellar variabilities can persist for decades (see also Paper I).

4.4. The variability associated with \( f_{32} \): the brightening in 2016 and other mass-loss indicators

The difference frequency \( f_{32} \) was not detected by ground-based observations; the value \( 0.09 \text{ c/d} \), reported by Ružič et al. (1994), is close to the first harmonic. The frequency \( f_{32} \) is the only peak in group \( g_0 \) that occurred in both 2015 and 2016. This frequency represents a variability in its own right as plain beat frequencies do not appear in power spectra. Figure 1 illustrates the difference well. The rise in amplitude of \( f_{32} \) at the end of the observations in 2016 sets in rather suddenly and after an extended period of quiescence. Similarly rapid rises and drops in the amplitude of \( \Delta \) frequencies have also been seen in 25 \( \psi^1 \) Ori (Baade et al. 2017b). A simple beating of two frequencies looks different.

During its maximum, the amplitude of \( f_{32} \) reaches a PTV value of 100 mmag. This is well outside the domain of non-radial pulsations in other B-type stars and exceeds the (time-independent; see Fig. 13) amplitude sum of its parent frequencies \( f_2 \) and \( f_3 \) by a factor of 4–5. Other stars with \( \Delta \) amplitudes above the sum of the parent amplitudes include \( \eta \) Cen (Paper I), 10 CMa, and 25 \( \psi^1 \) Ori (Baade et al. 2017b). Moreover, the variability with \( f_{32} \) is highly non-sinusoidal and the range above the inflection points of the light curve is much larger than that below (Fig. 1). This asymmetry and the large amplitude can be understood as near-circumstellar matter emitting extra light (Haubois et al. 2012; Baade et al. 2016). Such large-amplitude asymmetries have also been observed by BRITE Constellation in 25 \( \psi^1 \) Ori (Baade et al. 2017b). Because of the EER effects, it is not possible to infer the real photospheric amplitude associated with \( f_{32} \) and the above comparison of \( \Delta \)-frequency amplitude and parent \( g \)-mode amplitudes has no energetic meaning.

Figure 1 reveals another important detail. In the \( f_{32} \) cycle around mJD 630, several measurements appear up to \( \sim 100 \text{ mmag} \) below the upper envelope of the light curve. These measurements reach well below the mean brightness so that there is a temporary deficit of light. These fading should not be instrumental because both UBr and BTr independently recorded a similar, slightly weaker, event around mJD 198 (Fig. 1). The reality of this dimming is undoubtable. But the absence of simultaneous observations at all other times makes it impossible to assess the reality of any of the other, mostly much sparser, groups of bright and faint points. However, Figs. 9 and 10 point to increased scatter around extrema of the \( f_{32} \) light curve.

Comparable rapid switching between increased and attenuated brightness during phases of maximal \( \Delta \) amplitude has been observed by BRITE in 25 \( \psi^1 \) Ori (Baade et al. 2017b). This star has a spectral type and \( v \sin i \) similar to 28 Cyg such that it is also viewed from a similar perspective. One possible interpretation (cf. Sect. 4.1) is, therefore, that ejecta span some range in stellar latitude. The emission by the lifted-up matter is permanent (but not constant) whereas the only temporary removal of light implies strong variability in the amount of matter along the line of sight to the photosphere. This corroborates the conclusion that at the end of the BRITE observations in 2016 28 Cyg suffered a (small) series of mass ejections. That is, these brightenings probably were real outbursts.

With this behaviour of 28 Cyg (and 25 \( \psi^1 \) Ori) there are three ways in which a \( \Delta \) frequency can sculpt mass loss from Be stars:

1) Spectroscopy of \( \mu \) Cen (Rivinius et al. 1998a) has shown that major enhancements of the H\( \alpha \) line emission happen every time when the vectorial sum of at least two out of three specific NRP modes exceeds a threshold in amplitude.

2) In \( \eta \) Cen (Paper I), the mass loss is basically permanent as is suggested by the continuous presence of the \( \dot{\varepsilon} \) frequency in emission lines, which seems to be the response by the disc to mass transfer. The latter is continually modulated by \( f_{32} \) with minor apparently stochastic deviations superimposed.

3) The same may be at work in 28 Cyg but at a lower level (Fig. 9, Sect. 4.5). Much more prominent are single events spaced with the \( \Delta \) period. But the series of such events starts suddenly and, by inference from 25 \( \psi^1 \) Ori, also declines quickly; the observations of 28 Cyg in 2016 were terminated before the end of the active phase because the Sun was too close. This confirms the report by Tubbesing et al. (2000) that they saw only one H\( \alpha \) line-emission outburst and could rule out repetitions with \( f_{32} = 0.05 \text{ c/d} \) during their 100-d and 65-d observing windows.

It remains to be seen whether these three categories are genuine or the artefact of incomplete temporal sampling. There is no explanation of the timing of the brightenings in 28 Cyg. They may involve a third clock (in addition to \( f_2 \) and \( f_3 \)).

4.5. The nature of \( f_1 \) as a \( \dot{\varepsilon} \) frequency and other circumstellar variabilities

Paper I called the high-amplitude 1.56-c/d frequency of \( \eta \) Cen a \( \dot{\varepsilon} \) frequency after the discovery of this kind of variability (Stełł et al. 1998). In \( \eta \) Cen, the \( \dot{\varepsilon} \) frequency was spectroscopically detected (Rivinius et al. 2003). Typical \( \dot{\varepsilon} \) frequencies occur during outbursts, are best seen in emission lines and absorption lines formed high in the atmosphere, and – for unknown accidental reasons – appear to have values \( \sim 10^{-5} \) below the main spectroscopic frequency. Condensed to the capabilities of photometry, this is a good initial description of \( f_1 \) in 28 Cyg.

In \( \eta \) Cen, both amplitude and frequency of the \( \dot{\varepsilon} \) frequency are strongly variable and appear modulated with the \( \Delta \) frequency (Paper I). In 28 Cyg, the variations are also large but there is no regularity in the frequency, only a major perturbation just before the series of brightenings in 2016 (Figs. 8 and 12). This large frequency jitter is also reminiscent of Achernar, in which Goss et al. (2011) meticulously documented phase shifts of one of the two detected frequencies.

The maxima of the brightenings are roughly matched by strong amplitude maxima of \( f_1 \) (compare Figs. 1, 8, and 13). This is compatible with the spectroscopically established notion of Paper I. When an outburst or brightening occurs, the distribution of matter in the inner disc is not yet homogeneous (Baade et al. 1988; Hanuschik et al. 1991). The level of inhomogeneity reveals itself by the amplitude of the \( \dot{\varepsilon} \) frequency. As in \( \eta \) Cen and other Be stars observed by BRITE, \( f_1 \) is embedded in a frequency group (\( g_1 \); Figs. 7, 14, and 15) the strength of which is crucially related to that of the \( f_1 \). In 28 Cyg, a fair part of the neighbourhood of \( f_1 \) changes during a major brightening (Fig. 14). Both observations probably strengthen the notion that these apparent companion frequencies are circumstellar. On all these the grounds, the classification of \( f_1 \) as the \( \dot{\varepsilon} \) frequency of 28 Cyg appears safe.

At 9 \( M_\odot \), the model of Haubois et al. (2012) should be a good match to a B2 star such as 28 Cyg (cf. Harmance 1988). At the assumed typical fractional critical rotation rate of 80% (Frémat et al. 2005; Meilland et al. 2012; Rivinius et al. 2013) its equatorial radius is increased from 5.7 \( R_\odot \) to 6.5 \( R_\odot \). The
orbital radius of matter circling this star with the Štefl frequency, 1.4 c/d, amounts to 6.9 $R_\odot$. A comparison of the two radii not only supports the exophotospheric interpretation of the Štefl frequency but is also consistent with the model prediction that, at optical wavelengths, the emission from exophotospheric matter arises from a region measuring less than about two equatorial radii.

In spite of all these details, the net effect of the brightenings in 2016 remains uncertain. The event reported by Tubbesing et al. (2000) impacted a fair part of the disc. But the cadence of the spectroscopy did not trace accompanying star-disc connections. The BRITE photometry has the necessary sampling but cannot equally clearly distinguish between photospheric and exophotospheric variability. Photometry by BRITE and Hαos spectroscopy can be reconciled if the 1998 drop in Hα emission strength was caused by a short increase of the continuum flux similar to that recorded by BRITE in 2016. This would also be in good agreement with the models of Haubois et al. (2012).

The contemporaneous BeSS spectroscopy (Fig. 20) exhibits no direct counterpart of the photometric brightenings. A most sensitive indicator could be the wings of the Hα line emission. The effects of the high orbital velocity of, and Thomson scattering by, inner disc matter should both strengthen the wings (Baade 1986), but only in dense discs. At the time of the BeSS spectroscopy in 2016 the disc of 28 Cyg was only moderately developed. This probably explains why enhanced Hα wings were not detected (Fig. 19) in the wake of the brightening around mJD 630.

Figure 20 could be read as follows: at some moment, fresh matter was injected into the disc. With the help of viscosity, part of it drifted outwards but most of it lost angular momentum and fell back to the star. Because the disc is optically thick in Hα, the equivalent width did not change immediately after the outburst but only started to increase when the outwards drifting matter reached a domain that was not optically thick before. Since this region is farther away from the star and the disc is Keplerian, the separation of the emission peaks decreased.

This description is consistent with VDD hydrodynamic simulations coupled with radiative transfer calculations (Haubois et al. 2012). Figure 21 illustrates a periodic model (see Fig. 7 of Haubois et al. 2012), which alternates between one year of disc build-up at a fixed disc-feeding rate with one year of disc dissipation when the mass loss is shut off. At $t = 8$ yr, the outburst begins, replenishing the remnant of the disc from the previous two-cycle spread with fresh material. Initially the line equivalent width drops slightly, as a result of the increased EER continuum emission. But then this line equivalent width raises steadily and continues to grow past the cessation of the disc feeding at $t = 9$ yr owing to the quick decrease in the EER continuum emission. As observed in 28 Cyg (Fig. 20), the peak separation anti-correlates with line emission, but this is no longer true during disc dissipation.

Although $f_1$ exhibits large-amplitude variations, it never disappears completely. If Štefl frequencies are indeed close tracers of star-to-disc mass transfer, the implication is that this mass transfer was variable but permanent during the BRITE observations of 28 Cyg. Such a continuous, albeit variable, process may make larger contributions to the regular disc replenishment needed to overcome the demolishing effect of the viscosity than outbursts. This is another important commonality with η Cen (Paper I). It also seems supported by the persistence, for five months, of fairly strong wings of the not-so-strong Hα line emission (Fig. 19). Even in a late-type Be star, whose disc may additionally be truncated by a companion star, the Hα line emission forms over many stellar radii (Klement et al. 2015). Therefore, the inner disc volume, when well filled, acts as a buffer that is insensitive to minor variations of the mass inflow.

The amplitude of $f_1$ was also increased at the end of the observations in 2015 (Figs. 8 and 13) when there was no hint of a major brightening (Fig. 1). This might indicate that the steady mass-loss component can also lead to inhomogeneous mass distributions close to the star (unless due to intrinsic local instabilities), or the outburst was not strong enough to develop a disc.

Unless winds of Be stars originate from the circumstellar discs (Rivinius et al. 2013), in which case a direct link to pulsation is not expected, it would be interesting to repeat the simultaneous UV and optical spectroscopy by Peters & Gies (2000) to identify which of $f_1$, $f_2$, and $f_3$, if any, correlates with UV flux and wind. To date, in no Be star, including 28 Cyg, has precision photometry or spectroscopy found mass loss clearly modulated with the frequency of a single NRP mode. Instead, timescales 20–50 times longer (occurring as $\Delta$ frequencies) have been inferred. It would be useful to extend UV observations to this range and also to check for the distribution of the variability between sub- and super-escape velocities. The sampling should permit detection of the circumstellar $f_1$. 

![Fig. 21. Temporal evolution of the V-band brightness (top), Hα line equivalent width (middle), and peak separation (bottom) computed with the periodic model of Haubois et al. (2012), their Fig. 7) consisting of a series of one-year disc build-up phases followed by one-year dissipation phases. Solid, dotted, and dashed lines represent inclination angles 80°, 70°, and 60°, respectively. It should be noted that the difference in sign between the V magnitude changes at 80° and 60°. The outburst begins at $t = 8$ yr and ends at $t = 9$ yr.](image-url)
5. Conclusions and outlook

In the photometric variability of early-type Be stars some in-
cipient commonalities emerge as a set of frequencies that fol-
low a common pattern whose numerical values form the specific
fingerprint of every star. The top-level variability of 28 Cygni is
structurally the same as that of the very similar star η Cen
(Paper I):

(i) Most frequencies are concentrated in groups (Fig. 7).

(ii) Four frequencies dominate the short- and medium-term vari-
ability. They fall into three different categories:

(iii) Two spectroscopically confirmed g modes (f_2 and f_3,
Tubbesing et al. 2000).

(iv) One Štefl frequency (f_1), which originates from the star-
disc transition zone and is about 10% lower in value than f_2 and
f_3. This frequency may occasionally become undetectable, and
it can drastically increase around brightenings but does not con-
tribute to the brightenings (Fig. 13). Its frequency is much less
stable than the frequencies of the g modes (Figs. 8 and 12). But
its average value is roughly constant at all times.

(v) One ∆ frequency (f_{2,3,2}) of the two g modes. It has the
largest amplitude. During amplitude maxima, star-to-disc mass
loss seems increased as indicated by the enhancement of the Štefl
variability of emission lines in η Cen (Paper I; for 28 Cyg, see
Figs. 1, 9, and 10). This process may also be persistently modu-
lated with the ∆ frequency.

At this level, η Cen and 28 Cyg only differ in the numerical
values of the parameters quantifying the frequencies and their
amplitudes. Both stars also share the long-term persistence
of their basic variability patterns, including considerable amplitude
variations especially of f_1 and f_{2,3,2}.

The existence of a second star, such as η Cen, lends consid-
erable support to the description of the variability given in Pa-
er I. An inner “engine” clocked by the g modes and powered by
the ∆ variability lifts matter above the photosphere. In the inner
disc, a viscosity-controlled outer engine sorts the matter delivered to
it into two categories, namely super- and sub-Keplerian specific
angular momentum. Part of this process is observed as Štefl fre-
quency, the amplitude of which increases with the total amount
of inner-disc matter and its deviation from circular symmetry. It
is not yet possible to guess whether or not η Cen and 28 Cyg are
representative of a significant fraction of all early-type Be stars.

Walker et al. (2005, MOST), Huat et al. (2009, CoRoT), Neiner et al.
(2012, CoRoT), Kurtz et al. (2015, Kepler), and others have argued that the myriads of frequencies in Be stars
are due to pulsations. With so much support, this conclusion is not
to be dismissed lightly. However, Papers I and II of this se-
ries have suggested on several grounds that a circumstellar origin
may be a fairly reasonable alternative for a good part of this vari-
bility. The coming and going of many features in the frequency
spectrum also of 28 Cyg (Sect. 3.1.2 and Fig. 8) may also point
at the Štefl frequency as the tip of the iceberg.

Therefore, it makes sense to search for the key to the un-
derstanding of the Be phenomenon in the small set of anchor
frequencies instead of transient variations. Only for these fre-
quencies is there any plausible direct observed link to mass loss
(Figs. 1, 9, and 10). Ultimately, this requires that undulations of the
short-term variability can also explain disc life cycles of up to
a decade inferred from the Hα emission-line strength (taken as a
proxy of the total amount of matter in the circumstellar disc). In
28 Cyg, anchor frequencies have persisted for several decades,
which is long enough to allow such frequencies to contribute to
the explanation.

The simplest extrapolation in timescale to nearly a decade
(0.1 c/yr) would be a combination of modes with ∆ frequencies
of order 0.1 c/yr. However, viscosity does not let single big out-
bursts every 10 yr create photometric high states lasting several
years. In the VDD paradigm, a photometric high state of a disc
could result from outbursts with a frequency and effectiveness
sufficient to sustain a massive disc. The lowest level would be
formed by mini-outbursts with single ∆ frequencies. A second
clock could come into play for outbursts perhaps associated with
the brightening in 28 Cyg around mJD 630. At least a third level
would be required to regulate the first two processes and cause
cycles of a few years length. The example of the brightening
around mJD 630 illustrates that the amplitude amplification can be
a highly non-linear process, either in true NRP amplitudes or
their effect on mass loss or both.

One way of achieving slow clocking could be “hierarchical”
∆ frequencies, i.e. combinations of ∆ frequencies. In 28 Cyg,
they could be f_{2,3,2} and, if real, 0.00995 c/d (Sect. 3.1.2). In
their most basic form, these frequencies might explain seemingly
particularly simple cases as depicted in Fig. 5 of Keller et al. (2002)
in which long-lasting bright states cyclically repeat on two simi-
lar timescales of order 500–1000 d.

Irrespective of how several NRP wave patterns combine to
∆ frequencies, it seems plausible that for best coupling effi-
ciency their angular structures must be the same, i.e. they should
agree in their ℓ and m indices. In μ Cen (Rivinius et al. 1998b)
and 28 Cyg (Tubbesing et al. 2000) the available spectroscopic
evidence supports this expectation. The work of Rivinius et al.
(2003) has furthermore demonstrated that ℓ = −m = 2 modes
dominate the spectral variability of many Be stars. If equality
of the mode indices is a requirement for mass-loss-modulating
difference frequencies, this could be an important filter, mean-
ning that no two arbitrary NRP modes can combine to cause mass
loss. Indications of mass lift-ups occurring over some range in
stellar latitude may place first constraints on the pulsational ve-
locity field (ℓ and m). However, spectroscopic searches for ∆ fre-
quencies could be more effective in determining the geometry of
the variability. It would be desirable to learn from models
whether energy leakage from pulsations to mass loss can estab-
lish another effective filter of the NRP mode spectrum.

A robust distinction between stellar and circumstellar phe-
nomena is critical for the identification of frequencies for aster-
oseismology. High-cadence long-term space photometry has the
potential of achieving this. For the understanding of the Be phe-
nomenon at large, it is comforting that with the VDD model a
tool is available that permits observed circumstellar variations to
be cast into coherent sequences of dynamical states.

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