Superconductivity induced by structural reorganization in electron-doped cuprate NCCO

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Electron-doped and hole-doped superconducting cuprates exhibit a symmetric phase diagram as a function of doping. This symmetry is however only approximate. Indeed, electron-doped cuprates become superconductors only after a specific annealing process: This annealing affects the oxygen content only by a tiny amount, but has a dramatic impact on the electronic properties of the sample. Here, we report the occurrence of superconductivity in oxygen-deficient Nd$_{2-x}$Ce$_x$CuO$_4$ thin films grown in oxygen-free environment, after annealing in pure argon flow. As verified by x-ray diffraction, annealing induces an increase of the interlayer distance between CuO$_2$ planes in the crystal structure. Since this distance is correlated to the concentration of oxygens in apical positions, and since oxygen content cannot substantially increase during annealing, our experiments indicate that the superconducting phase transition has to be ascribed to a migration of oxygen ions to apical positions during annealing. Moreover, as we confirm via first-principles density functional theory calculations, the changes in the structural and transport properties of the films can be theoretically described by a specific redistribution of the existing oxygens ions at apical positions with respect to CuO$_2$ planes, which remodelates the electronic band structure and suppresses the antiferromagnetic order, allowing the emergence of hole superconductivity.

Since the discovery of superconductivity in LaBaCuO by Bednorz and Müller in 1986 [1], the family of high-temperature cuprate superconductors has grown to include more than hundreds compounds [2] with temperatures as high as 133 K at atmospheric pressure [3]. All these compounds share a similar crystal structure, made up of stacked layers of copper-oxygen planes, and fit into a universal phase diagram, where superconductivity emerges upon doping an antiferromagnetic Mott insulator [4, 5]. Indeed, when the stoichiometric parent compound is doped via ionic substitution, the antiferromagnetic phase is suppressed and superconductivity appears. Ionic substitution may result in the creation of additional holes or electrons in the CuO$_2$ planes. Hole-doped [1–3] (e.g., La$_{2-x}$Sr$_x$CuO$_4$) and electron-doped [6–10] (e.g., Nd$_{2-x}$Ce$_x$CuO$_4$) share a similar temperature-doping phase diagram, which indicates a common origin of the superconducting pairing. However, the symmetry between hole- and electron-doped cuprates is only approximate. For example, superconductivity in electron-doped cuprates is much harder to achieve, since the antiferromagnetic phase persists at higher doping levels [8, 9, 11–13].

Perhaps the most puzzling anomaly of electron-doped cuprates is the fact that doping alone does not produce superconductivity [8, 9, 14]. As-grown samples are antiferromagnetic Mott insulators, and become superconducting only after high-temperature oxygen-reducing annealing [6, 7]. Annealing reduces the oxygen content by a small fraction [15–20] (between 0.1% and 2%), which contributes to additional electrons in the CuO$_2$ layers [11, 12, 21–25], and to a decrease of the interlayer distance [26–31]. This results in a dramatic change of the electronic properties [32–38], including the emergence of the superconducting transition and a reduction of the Néel temperature [11, 39, 40], which cannot be achieved only by doping (e.g., by addition of extra cerium in Nd$_{2-x}$Ce$_x$CuO$_4$ [29]). Furthermore, single crystals of the undoped parent compound Nd$_2$CuO$_4$ are never superconducting. Conversely, Nd$_2$CuO$_4$ thin films exhibit superconductivity after annealing, even without doping [14, 29]. In all cases, the annealing process must be carried in rather specific conditions that drive the samples almost to the limit of decomposition [41, 42]. For these reasons, it is clear that the annealing process must have additional effects. These may be the consequence of a reorganization of the crystal structure and/or a change in the distribution of dislocations and defects in the sample, such as the removal of the interstitial apical oxygens (defects) [17, 43–45], the removal of intrinsic in-plane oxygens [46–48], or the migration of copper ions to repair and reduce copper vacancies [49, 50]. A measurable effect of annealing is the change of the c-axis lattice parameter, which is 2 times the interlayer distance between CuO$_2$ planes: The lattice parameter decreases to an optimal value cSC at which superconductivity appears [14, 51]. Generally, oxygen reduction produces a decrease of the c-axis lattice parameter associated with the removal of apical oxygen [17, 18]: Hence, the value of c has been considered as a qualitative measure of the oxygen content [28, 30, 31].

In this work, we report the occurrence of superconductivity in oxygen-deficient Nd$_{2-x}$Ce$_x$CuO$_4$ (NCCO) thin films, ob-
tained by annealing in oxygen-free atmosphere, and we provide a theoretical framework to describe the electronic properties and the structural changes before and after annealing. Our samples are grown by DC sputter deposition in oxygen-free atmosphere, and exhibit a $c$-axis lattice parameter shorter than the optimal value $c_{SC}$, which indicates oxygen deficiency, and the presence of a negligible amount of apical oxygens. Remarkably, these samples become superconducting after annealing in pure argon atmosphere, with a simultaneous increase of the $c$-axis parameter. This strongly indicates that the superconducting phase transition cannot be ascribed to a change of the oxygen content, but to a microscopic reorganization of the crystal structure induced by annealing. Moreover, in order to obtain a complete phase diagram as a function of the $c$-axis lattice parameter, we have grown thin films also in oxygen/argon atmosphere. These samples exhibit a $c$-axis lattice parameter longer than the optimal value $c_{SC}$ and, as expected, become superconducting after annealing, with a decrease of the $c$-axis, in agreement with previous studies [6–9]. In all samples, the superconductivity is established only after the $c$-axis parameter reaches the optimal value $c_{SC} = 12.08\,\text{Å}$. As we show using first-principles density functional theory (DFT), the evolution of the $c$-axis parameter and the presence of holes can be explained in terms of a microscopic structural modification, i.e., with existing oxygens ions partially migrating to apical positions with respect to CuO$_2$ planes. This induces a remodulation of the energy bands and the suppression of antiferromagnetic order, allowing the emergence of hole superconductivity, i.e., the pairing of hole carriers within the same electronic band [34, 37, 38].

The undoped NCCO parent compound Nd$_2$CuO$_4$ crystallizes in a tetragonal $T'$ crystal structure, containing CuO$_2$ layers stacked along the $c$ axis and sandwiched between the charge reservoir layers, as shown in Fig. 1(a). Moreover, it is well-known that the lattice structure of NCCO thin films and other electron-doped materials exhibit disorder, with the presence of oxygen vacancies at regular sites (CuO$_2$ layers or charge reservoir layers) as well as excess oxygen at apical sites above and below CuO$_2$ layers [8, 9, 14], as shown in Fig. 1(b). In particular, the presence of in-plane oxygen vacancies is correlated to an increase of electrons in the conduction band [11, 12, 21–23, 25], whereas the concentration of oxygen ions on apical sites is correlated with the elongation of the $c$-axis parameter [28, 30, 31].

In our experiment, we used optimized DC sputtering to grow well-oriented NCCO films without spurious phases and with a fixed cerium content $x = 0.17 \pm 0.01$. We obtained films with thickness in the range 50–100 nm, grown respectively in pure argon (type A samples) and mixed argon/oxygen atmosphere with ratio $O_2/Ar > 1\%$ (type B samples), at a total pressure of 1.7 mbar and heater temperature of 850 °C (see also Ref. 52 and 53 and Supplemental Material [54]).

In order to analyze the effect on the crystal structure of the reducing thermal treatment inducing superconductivity, the in-plane and the out-of-plane lattice parameters $a$, $b$, and $c$ are measured before and after annealing by x-ray diffraction (XRD). We found for the as-grown type A samples $c = 12.04–12.07\,\text{Å}$ and $a = b \approx 3.95–3.96\,\text{Å}$, while for the as-grown type B samples $c = 12.09–12.15\,\text{Å}$ and $a = b \approx 3.94–3.97\,\text{Å}$. After annealing, type A samples grown in oxygen-free atmosphere exhibit a slight elongation of the $c$-axis, whereas the in-plane lattice parameter remains unchanged. Conversely, type B samples grown in oxygen atmosphere exhibit a systematic decrease of the $c$-axis after annealing, in agreement with previous results [26–31], and a small change of the in-plane lattice parameter in some of the samples. The analysis of $(00l)$ reflections in XRD patterns [54] allows to obtain the $c$-axis lattice parameter of all superconducting films to be $c_{SC} = 12.080–12.088\,\text{Å}$. As established by extensive studies on electron-doped films fabricated by molecular-beam epitaxy [55–57] and pulsed laser deposition [58–61], the $c$-axis lattice parameter can be used as a measure of the oxygen content. In these studies, the $c$ parameter is always larger than the optimal superconducting value $c_{SC}$, as we also observe in type B over-oxygenated samples, and decreases with the concurrent elimination of excess oxygen atoms during annealing. Hence, a value $c < c_{SC}$ in type A samples indicates oxygen-deficiency.

We measured the temperature dependence of the in-plane resistivity $\rho(T)$ with a four-probe method in the temperature range 1.6–300 K, before and after annealing. As-grown nonsuperconducting type A samples (fabricated in oxygen-free atmosphere) exhibit a crossover between metallic and insulating regimes identified by a minimum of the resistivity $\rho(T)$ at temperature $T_{min}$, and with a residual resistivity ratio $RRR = \rho(300\,\text{K})/\rho(4.2\,\text{K}) > 1$, as shown in Fig. 2(a). Furthermore, the resistivity exhibits a quadratic temperature dependence in the metallic region above $T_{min}$, as

![FIG. 1. (a) The NCCO parent compound (undoped Nd$_2$CuO$_4$) crystallizes in the tetragonal $T'$ structure. CuO$_2$ layers are sandwiched between the charge reservoir Nd$_2$-Ce$_2$O$_2$ layers. Copper ions are surrounded by a square planar arrangement of oxygen ions in the $ab$ plane. Oxygen ions are located within the CuO$_2$ layers and the charge reservoir layers. (b) In doped compounds, oxygen ions may partially occupy apical sites above or below the Cu atoms, e.g., one apical oxygen for every two copper atoms, or every copper atom ($T'$ structure). The concentration of apical oxygens is correlated to the elongation of the $c$-axis parameter.](image-url)
it is clearly visible in Fig. 2(a). In electron-doped compounds, a quadratic resistivity dependence is usually found even above room temperature [8, 10, 62, 63]. As-grown nonsuperconducting type B samples (fabricated in mixed argon/oxygen atmosphere) exhibit instead a weak semiconductor-like temperature dependence on the resistivity with $\rho(T) \propto R(T) \propto T^{-\alpha}$, as shown in Fig. 2(b).

The main effects of annealing are the modification of the oxygen content and the structural reorganization and redistribution of crystal defects and dislocations. In order to disentangle these two effects, we performed an ex-situ annealing in oxygen-free, pure argon flow. Despite different environmental growth conditions and different structural and electrical properties of type A and B samples, similar thermal treatments are needed to induce superconductivity. All samples become superconducting after annealing at high temperatures 900–950 °C, with 0.5–2 hours annealing time, depending on the film thickness. Moreover, all samples have similar critical temperatures $T_c \lesssim 24$ K, as shown in Fig. 2(c). In contrast, no superconducting transition and no structural change are detected after annealing at temperatures below 900 °C and with the same environmental conditions, as reported elsewhere [64].

Figure 2(d–e) shows the phase diagram of our NCCO samples as a function of the $c$-axis lattice parameter, before and after annealing, which is the main experimental result of this work. In particular, Fig. 2(d) shows the residual resistivity ratio $RRR$ as a function of the $c$-axis lattice parameter. In the region $c < c_{SC}$ (sample type A), samples behave as weakly disordered metal with $RRR \gtrsim 1$ and exhibit a metal-insulator crossover with minimum resistivity at $T_{min}$. We observe values of $T_{min}$ up to 250 K and $RRR \approx 1–2$, with $RRR$ increasing with decreasing $T_{min}$. In the region $c > c_{SC}$ (sample type B), samples behave as disordered systems with $RRR \lesssim 1$, with a weakly semiconductor-like temperature dependence on the resistivity. Most importantly, Fig. 2(e) shows the superconducting critical temperatures $T_c$ as a function of the $c$-axis lattice parameter. All samples achieve superconductivity after high-temperature annealing, accompanied by a structural change: An increase of $c$-axis for type A samples and a decrease for the type B samples. The superconducting regime is restricted to the value of lattice constant $c_{SC} = 12.08$ Å. Hence, high-temperature annealing not only induces superconductivity, but also a concurrent and systematic increase (in type A samples) or decrease (in type B samples) of the $c$-axis lattice parameter toward the optimal value $c_{SC}$. This strongly suggests that the superconducting phase transition is induced by a structural reorganization and redistribution of oxygen atoms within the CuO$_2$ layers, charge reservoir layers, and in the apical positions. Moreover, the correlation between the concentration of apical oxygens and the $c$-axis parameter clearly points to the crucial role and impact of apical oxygens on the electronic properties of the compound after annealing.

In order to understand the role of the structural reorganization of oxygen atoms, and in particular the effects of the presence/absence of apical oxygens on the properties of the three types of samples, we have theoretically modeled and studied the system by DFT using the VASP [65] package with plane-wave basis set and projector augmented wave method [66]. In particular, as-grown type A samples have been modeled by a $T'$ structure as in Fig. 1, i.e., a crystal structure with no apical oxygens, according to its fabrication in oxygen-deficient atmosphere. Then, as-grown type B samples have been instead modeled by a $T'$ structure, i.e., a crystal structure with one apical oxygen for every copper atom, according to its fabrication in oxygen-rich atmosphere. Finally, superconducting samples have been modeled by a mixed $T_{SC} = 2T^* + T'$ structure, with two $T^*$ cells and one $T'$ cell alternating along the $c$-axis, i.e., a crystal structure with two apical oxygens for every three copper atoms. This is justified by the experimental evidence that the $c$-axis lattice parameter and, consequently, the number of apical oxygens, assume intermediate values between those measured for type A and B samples. DFT calculations have been performed by first relaxing the crystal structure in order to obtain the lattice parameters and compare them with the actual ones and, in particular, with their characteristic hierarchical order. We also computed the antiferromagnetic moments $m$ in order to monitor the intensity of the antiferromagnetic correlations, that could prevent

**FIG. 2.** (a) Resistivity as a function of temperature for type A samples, plotted on a log-log scale and normalized to the value of the minimum of the resistivity. (b) Resistance as a function of temperature for type B samples, plotted on a log-log scale. Continuous lines $R(T) \propto T^{-\alpha}$ are the best fit to the data with slopes $\alpha = 0.54, 0.72, 0.79, 0.98$. (c) Normalized resistivity as a function of temperature for type A and B samples after annealing, showing the superconducting transition at $T_c \lesssim 24$ K. (d) Residual resistivity ratio $RRR$ for as-grown samples (both types) and (e) superconducting critical temperature $T_c$ of samples after annealing, as a function of the $c$-axis lattice parameter. The dashed gray line corresponds to the average value of $c_{SC}$ and the continuous smooth curve is a guide for the eye.
the emergence of superconductivity. The study of the $T'$ and $T^*$ phases of the undoped Nd$_2$CuO$_4$ is reported in the Supplemental Material [54]. The $T^*$ phase shows a larger band gap compared with the $T'$ phase. The more correlated behavior of the $T^*$ is confirmed by the magnetic moments, which are $m = 0.38\mu_B$ and $m = 0.43\mu_B$ for the $T'$ and $T^*$ phases respectively. Regarding the doped phase, Fig. 3(a) and (b) show the results for the $T^*$ structure for $x = 0.125$ and $x = 0.25$, respectively. In both cases, and reasonably for all intermediate doping (including $x = 0.17$), we have (i) a quite large indirect band gap $\Delta E_{XM}$ between the maximum of the lower Hubbard band at the point X (hole pocket) and the minimum of the upper Hubbard band at the point M (electron pocket), (ii) strong antiferromagnetic correlations ($m = 0.34\mu_B$ and $0.24\mu_B$, respectively, for $x = 0.125$ and 0.25), and (iii) hole pockets away from the Fermi level. This strongly correlated scenario accounts for the insulating behavior of as-grown type B samples. Figure 3(c) shows the results for the $T'$ structure for $x = 1/6 \approx 0.17$. The gap $\Delta E_{XM}$ has practically disappeared, although the antiferromagnetic correlations are still quite large ($m = 0.27\mu_B$). However, hole pockets are still far from the Fermi level. Such a scenario accounts for the (poor) metallic behavior of as-grown type A samples. Finally, Fig. 3(d) shows the results for the $T_{SC}$ structure for $x = 1/6$. The gap $\Delta E_{XM}$ has completely disappeared, as well as the antiferromagnetic correlations for the $T'$ region ($m = 0.04\mu_B$), and hole pockets are available right at the Fermi level (at the symmetry point X). However, antiferromagnetic correlations in the $T^*$ portion of the material are still relevant, being $m = 0.36\mu_B$. The presence of holes at the Fermi level and the suppression of antiferromagnetic correlations are fully compatible and can explain the emergence of hole superconductivity [34, 37, 38] in all samples after annealing. Moreover, confirming the validity and accuracy of the chosen modelization and the consistency of the obtained results, the relaxed values of the $a$ and $c$-axis lattice parameters for $x = 1/6$ are close to the experimental ones and, more importantly, in the same hierarchical order: For the $T'$ structure (as-grown type A samples) $a = b = 3.91\text{Å}$ and $c = 12.01\text{Å}$, for the $T^*$ structure (as-grown type B samples) $a = b = 3.83\text{Å}$ and $c = 12.26\text{Å}$, and for the $T_{SC}$ structure (superconducting samples) $a = 3.85\text{Å}$ and $c = 12.18\text{Å}$. The variation of the $c$-axis lattice parameter can be understood in terms of level repulsion between the bands with dominant $T'$ character and those with dominant $T^*$ character [see Fig. 3(d)] that leads to a remodulation of the overall band structure, which definitely weakens the antiferromagnetic correlations of the $T'$ region and allows the emergence of holes right at the Fermi level (more details in the Supplemental Material [54]).}

Concluding, the structural and the transport properties of NCCO samples shed new light on the microscopic mechanism underlying the annealing process, which is responsible for the onset of the superconductivity. Indeed, our experiments indicate that the removal of the excess oxygen is not sufficient to trigger superconductivity: Our oxygen-deficient samples, grown in oxygen-free atmosphere, become superconducting only after high-temperature annealing, which always occurs together with a change of the $c$-axis lattice parameter. This strongly indicates that the superconducting phase transition is induced by a microscopic structural reorganization, even in almost-optimally doped samples. This conclusion is supported by our theoretical analysis. Indeed, our DFT calculations show that the presence of a sizable number of apical oxygens is necessary to allow the emergence of hole superconductivity. In particular, no apical oxygens ($T'$ structure), or too many of them ($T^*$ structure), stabilize strong antiferromagnetic correlations and keep hole states away from the Fermi level, whereas an intermediate number of apical oxygens ($T_{SC}$ structure) induces a suppression of antiferromagnetic correlations and allows to have holes available right at the Fermi level. This points to the relevance of interlayer hoppings mediated by apical oxygens, analogously to the scenario evidenced in hole-doped cuprates [67, 68]. Our experimental investigation and theoretical analysis provide strong evidence that the superconducting phase transition in electron-doped NCCO superconductors cannot be explained only in terms of changes of the oxygen content, but it necessarily requires a structural reorganization of the oxygen atoms in apical positions, which deeply affects the electronic properties of the compound.

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![FIG. 3. DFT electronic band structure of NCCO for: (a) $T^*$ structure with $x = 0.125$, (b) $T^*$ structure with $x = 0.25$, (c) $T'$ structure with $x = 1/6 \approx 0.17$, and (d) $T_{SC} = 2T^* + T'$ structure with $x = 1/6$, where we highlighted the dominant $T'$ and $T^*$ bands with larger contributions. The Fermi level is set to zero. The flat bands at 0.5–1.5 eV above the Fermi level are the cerium 4f bands. All other lower-energy bands are copper 3d bands.](image-url)
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Superconductivity induced by structural reorganization in electron-doped cuprate NCCO:
Supplemental Material

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In this Supplemental Material, we include detailed information on the sample preparation, X-ray diffraction measurements, and computational details.

SAMPLE PREPARATION

Nd2−xCexCuO4 (NCCO) films with a fixed cerium content in the range 0.16–0.18 have been grown on (100) SrTiO3 substrates by DC sputtering technique. A single target of the stoichiometric Nd1.85Ce0.15CuO4 compound has been used as a sputtering source in an on-axis configuration with the substrate [1]. Films with thickness in the range 50–100 nm have been fabricated in pure argon (type A samples) or in mixed atmosphere of argon and oxygen (O2), with ratio O2/Ar > 1% (type B samples), both at a total pressure of 1.7 mbar and at a heater temperature of 850 °C. A first in-situ annealing is performed with a dwell time of 30 minutes at the same deposition temperature. In both cases, the superconductivity of the films was observed after a suitable ex-situ thermal treatments in flowing argon at a temperature above 900–950 °C. Despite different deposition conditions, the high annealing temperature is the same for all films, while an annealing time in the range 0.5–2 hours is used, depending on the film thickness.

Morphology, phase composition, and sample purity were inspected by scanning electron microscopy combined with wavelength-dispersive spectroscopy [1, 2], using an Oxford Scanning Electron Microscope Leo EVO 50 equipped with a wavelength-dispersive spectrometer. Structural properties are obtained by high-resolution X-ray diffraction technique in a Philips X’Pert-MRD diffractometer equipped with a four-circle cradle.

The electrical transport properties were investigated in a Cryogenic Ltd. cryogen-free cryostat equipped with an integrated cryogen-free variable-temperature insert operating in the range 1.6–300 K. In this system, the sample is cooled by a continuous helium gas flow and the temperature stability is within 0.01 K. Sample temperature is measured via a LakeShore Temperature Controller model 350 connected to a LakeShore Cernox sensor. The electrical resistance measurements as a function of the temperature have been performed by a four-probe method, using a Keithley model 2430 as current source and a Keithley model 2182 as voltage meter. On selected films, in order to evaluate the resistivity, we realized microbridges with length L = 1 mm, width W = 100 μm using a standard UV photolithography and wet etching in a 1% solution of H2PO4 in pure water.

X-RAY DIFFRACTION MEASUREMENTS

The structural properties of DC-sputtered NCCO films have been investigated by X-ray diffraction (XRD) technique. Figure S1 reports the typical θ-2θ pattern of as-grown type A, as-grown type B, and superconducting samples. Besides the substrate reflections, XRD patterns of as-grown, nonsuperconducting samples show only the four (00l) diffraction peaks with l = 2, 4, 6, 8, which are characteristic of the T’ tetrago-

![X-ray diffraction patterns](https://example.com/x-ray-patterns.png)
nal crystal structure, indicating a preferential growth with the c-axis perpendicular to the film surface and the absence of spurious phases.

The analysis of the $(00l)$ reflections allows to obtain directly the c-axis lattice parameter from the Bragg law, $2d \sin \theta = \lambda$, with $\lambda = 1.54056 \text{Å}$, $\theta$ the half of the angular peak position $2\theta$, and with $d = c/l$ in this case. Insets of Fig. S1 report the quantity $2 \sin \theta / \lambda$ as a function of the Miller index $l$ together with the linear best fit of the data. The fitting parameter gives a different c-axis parameter for each sample. In particular, the c-axis parameter measured in the superconducting sample is $c_{SC} = 12.079 \pm 0.005 \text{Å}$. The value $c = 12.069 \pm 0.005 \text{Å}$ obtained for the type A film is shorter than $c_{SC}$, while the c-axis parameter of the type B sample is $c = 12.09 \pm 0.01 \text{Å}$ of the type A sample is longer. Hence, the most oxygenated type B samples behave as typical samples reported in previous studies, where the measured as-grown c-axis parameter is longer than the value measured in superconducting samples [3–8]. A value $c < c_{SC}$ is the peculiarity of our type A films.

Figure S2 shows the angular positions $2\theta$ of the (004), (103), and (114) peaks respectively [(a) to (c)], for one type A and one type B as-grown samples compared with the value measured after annealing. We found for the as-grown type A sample $c = 12.04 \pm 0.01 \text{Å}$ and $a, b = 3.96 \pm 0.01 \text{Å}$, while for the as-grown type B samples $c = 12.11 \pm 0.01 \text{Å}$, $a, b = 3.94 \pm 0.02 \text{Å}$.

Figure S2(d) reports the measurement of the mosaicity of type A and B samples by the $\omega$-scan around the (004) reflection: $\omega$ is the x-ray incident angle. Type A and B samples show a full width at half maximum (FWHM) equal to $0.5^\circ$ and $0.6^\circ$ respectively, indicating a more uniform c-axis orientation for type A samples (i.e., better epitaxial growth).

**COMPUTATIONAL DETAILS**

We have performed first-principles density functional theory (DFT) calculations by using the VASP [9] package based on plane-wave basis set and projector augmented wave (PAW) method [10]. A plane-wave energy cut-off of 450 eV has been used for the atomic relaxation and 530 eV for the other calculations. A $k$-point grid of $8 \times 8 \times 2$ has been used for the atomic relaxation and $10 \times 10 \times 4$ for the other calculations. For the treatment of exchange-correlation, Perdew-Burke-Ernzerhof [11] generalized gradient approximation for solid has been considered, since it is accurate for the structural relaxation of the $A_2BO_4$ oxides bulk [12].

The analysis of the structural phases of compounds with $4f$-electrons is a nontrivial problem in DFT due to the difficulties to catch the position of the energetic levels of the $f$-electrons [13]. Few works studied electron-doped cuprate superconductors using ab initio techniques. Considering $4f$ electrons in the core level, Bansil and coworkers were able to obtain the correct insulating groundstate for the undoped cases [14–16]. We use the PAW with 3 frozen $f$-electrons for the Nd and without frozen $f$-electrons for the Ce. Using the PAW without frozen electrons for the Ce, the $T^*$ phase is always the ground state. Using the PAW with three frozen $f$-electrons for the Ce, we obtain the stabilization of the $T^*$ phase, but this does not allow the Ce$^{4+}$ configuration experimentally observed.

We included the effects of the Hubbard $U$ on the Cu sites. We scanned the values of $U_{Cu}$ from 1 to 4 eV for the undoped and used $J_H = 0.15U$ for the Cu-3$d$ states, and we assumed the value of $U_{Cu} = 3.2$ eV because for this value the undoped $T^*$ phase is a narrow gap semiconductor. The Coulomb repulsion was applied also on the rare earth Nd and Ce (4$e$) and O (6$e$) but it is much less relevant since these electrons are far from the Fermi level.

To account the G-type antimagetism in Nd$_2$CuO$_4$ we use a $\sqrt{2} \times \sqrt{2} \times 2$ supercell with 4 formula units. To investigate the structural properties as a function of doping, an additional calculation was done in the overdoped regime at $x = 0.25$. Using Vegard’s law, we estimated the lattice constants for $x = 0.17$, which correspond to almost-optimally doping (as in our samples). Once we understood the structural properties, we study the electronic and magnetic properties of the compound relative to a value of the doping close to the experimental one. In order to do so, we used a $\sqrt{2} \times \sqrt{2} \times 3$ supercell with 6 formula units. One Ce atom in 6 formula units will give the concentration of $x = 1/6 \approx 0.17$. This supercell can host 3 cuprate layers. However, in order to reproduce the $T^*$ phase we need an even number of layers. As a consequence, the...
\( \sqrt{2} \times \sqrt{2} \times 3 \) supercell cannot host the T+ phase but it can host the T' phase and a mixed phase with two T+ cells and one T' cell alternating along the c-axis. In this work, we call this phase the TSC = 2T+ + T' phase.

The most stable configuration of the Ce atoms is obtained when the Ce atoms are far from each other. This means that during the growth the Ce atoms have a tendency to avoid each other, which points to a homogeneous distribution of these Ce atoms during the growth. In the most stable configuration of T' phase, the Ce atoms are not in the apical oxygen layer. In the most stable configuration of the mixed TSC phase, the Ce atoms are closer to the CuO2 layers of the T' phase.

**DFT STUDY OF UNDOPED Nd2CuO4**

In this Section, we present the results of the undoped Nd2CuO4. The T' and T+ phases of the Nd2CuO4 have the same stoichiometry but a different atomic position of the oxygen atoms and consequently of the atomic layers. The T' phase consists of 4 atomic layers CuO2/ONdO/NDnO while the T+ contains 3 atomic layers CuO2/O d'NdO/NDnO. The different atomic composition of the atomic layers has a large influence on the lattice constant \( c \) and consequently on the in-plane lattice constant too. Considering just the effect of the packaging, we would expect that the T' phase with 4 atomic layers should have a larger lattice constant, but we also need to consider the effect of the charge. In an oversimplified ionic picture, the CuO2 layers have a total charge \( -2 \), the O layers have charge \( -2 \), the Nd2 layers have charge +6 while the NdO layers have charge +1. Therefore, the 4 layers of the T' phase have charge \( -2/ - 2/ +6/ -2 \) while the 3 layers of the T+ phase have \( -2/ +1/ +1 \). Due to the greater charge, the 4 layers of the T' phase attract each other much more than the 3 layers of the T+ phase resulting in a shorter c-axis of the T' phase. Therefore, there is an interplay and competition between the charge and the volume effect: As a result, the T' phase has a shorter c-axis than the T+ phase. As a consequence of the shorter c, the T' phase presents a larger value of the in-plane lattice constant \( a \). This simplified picture was verified in our DFT results. We performed structural relaxation for the undoped case for the T' and T+ phases. We obtained \( a = 3.91 \) Å and \( c = 12.12 \) Å for the T' phase: The total volume is 92.7 \( \text{Å}^3 \) per formula unit. We obtained \( a = 3.83 \) Å and \( c = 12.34 \) Å for the T+ phase: The total volume is 90.3 \( \text{Å}^3 \) per formula unit.

The Cu states in T+ are more ionic due to the larger number of nearest-neighbor oxygen atoms, indeed the Cu d-orbitals are more localized and therefore the T+ phase is more insulating. Instead, the T' phase is a semiconductor. Once we fixed the equilibrium atomic positions, we investigate the electronic properties scanning the value of U_{Cu}. We search for the critical value of \( U_{Cu}^{SC} \) such that the T+ phase is insulating, we get the value \( U_{Cu}^{SC} = 3.2 \text{ eV} \) for the T' phase and we assume this value for all the following calculations. The band structure of the semiconducting T' phase is shown in Fig. S3(a). We have the completely unoccupied upper Hubbard band between 0 and +2.2 eV above the Fermi level due to the \( x^2 - y^2 \) orbital in the minority spin channel. The lower Hubbard band due to the \( x^2 - y^2 \) orbital in the majority spin channel is completely occupied and entangled with other occupied Cu d-bands. The band structure shows an indirect band gap with the maximum of the valence band at the X point and the minimum of the conduction band at the M point. The gap in the DFT approach is opened by the interplay between \( U_{Cu} \) and the antiferromagnetic order: Indeed, the T' phase without magnetism shows a metallic phase with robust holes at the X point as shown in Fig. S3(b). In the nonmagnetic phase, we also have a nonsymmetric symmetry that produces a double degenerate band along the MX direction and a semi-Dirac point in X. Performing the antiferromagnetic calculation for the T+ phase, we obtain the band structure shown in Fig. S3(c). The band structure of the T+ phase shows a larger band gap and flatter Cu d-bands, but for the rest, we have the same properties as in the T' phase.

At \( U_{Cu} = 3.2 \text{ eV} \), the energy difference between the antiferromagnetic and nonmagnetic phase is 22 meV per formula unit for the T' phase and 70 meV per formula unit for the T+ phase. Therefore, the T+ phase has a larger gap and its antiferromagnetic ground state is more robust. Increasing the value of \( U \), the antiferromagnetic phase will become more stable but the scenario described here does not change qualitatively.
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