Sterile neutrino decay as a common origin for LSND/MiniBooNe and T2K excess events

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We point out that the excess of electron-like neutrino events recently observed by the T2K collaboration may have a common origin with the similar excess events previously reported by the LSND and MiniBooNE experiments and interpreted as a signal from the radiative decays of a sterile neutrino $\nu_h$ with the mass around 50 MeV produced in $\nu_\mu$ neutral current (NC) interactions. In this work we assumed that the $\nu_h$ can also be produced in $\nu_e$ NC reactions.

Over the past 10 years there is a puzzle of the 3.8 $\sigma$ event excess observed by the LSND collaboration [1]. This excess originally interpreted as a signal from $\bar{\nu}_\mu \to \bar{\nu}_e$ oscillations was not confirmed by further measurements from the similar KARMEN experiment [2]. The MiniBooNE experiment, designed to examine the LSND effect, also found no evidence for $\nu_\mu \to \nu_e$ oscillations. However, an anomalous excess of low energy electron-like (e-like) events in quasi-elastic neutrino events has been observed [3]. New MiniBooNE results from a search for $\bar{\nu}_\mu \to \bar{\nu}_e$ oscillations also show an excess of events, which has a small probability to be identified as the background-only events [4]. The data are found to be consistent with $\bar{\nu}_\mu \to \bar{\nu}_e$ oscillations in the 0.1 eV$^2$ range and with the evidence for antineutrino oscillations from the LSND.

In the recent work [5] (see also [6–8]) it has been shown that puzzling LSND, KARMEN and MiniBooNE results could all be explained in a consistent way by assuming the existence of a heavy sterile neutrinos ($\nu_h$). The $\nu_h$ is created in $\nu_\mu$ neutral-current interactions and decay subsequently into a photon and a lighter neutrino $\nu$ in the LSND and MiniBooNE detectors, but it cannot be produced in the KARMEN experiment due to the high energy threshold. The $\nu_h$ could be Dirac or Majorana type, and it could be produced, e.g. through the $\nu_\mu \to \nu_h$ mixing. The $\nu_h$ could decay dominantly into $\gamma \nu$ pair if, for example, there is a large enough transition magnetic moment between the $\nu_h$ and $\nu$ mass states. Such kind of $\nu_h$’s may be present in many interesting extensions of the standard model, see e.g. [9]. Assuming the $\nu_h$ is produced through mixing with $\nu_\mu$, the combined analysis of the LSND and MiniBooNe excess events suggests that the $\nu_h$ mass, mixing strength, and lifetime are, respectively, in the range

$$40 \lesssim m_h \lesssim 80 \text{ MeV}, \quad 10^{-3} \lesssim |U_{\mu h}|^2 \lesssim 10^{-2},$$

$$10^{-11} \lesssim \tau_h \lesssim 10^{-9} \text{ s}. \quad (1)$$

A detailed discussion of consistency of these values with the constraints from previous searches for heavy neutrinos [10] as well as of the interpretation of the $\nu_h$ decay in terms of transition magnetic moment is presented in [5, 8]. Briefly, the mixing of $\nu_h$ is not constrained by the limits from the most sensitive experiments searched for extra peaks in two-body $\pi, K$ decays [11], because the $\nu_h$ mass range of $\nu_h$ is outside of the kinematical limits for $\pi_{\mu 2}$ decays, and not accessible to $K_{\mu 2}$ experiments due to experimental resolutions. The parameter space of $\nu_h$ cannot be ruled out by the results of high energy neutrino experiments, such as NuTeV or CHARM, as they searched for $\nu_h$’s of higher masses ($m_h \gtrsim 200$ MeV) decaying into muonic final states ($\mu \pi \nu, \mu \mu \nu, \mu e \nu, \ldots$) [10], which are not allowed in our case. The best limits on $|U_{\mu h}|^2$ derived for the mass range $\nu_h$ from the search for $\nu_h \to e^+ e^- e^+ e^-$ decays in the PS191 experiment [11], as well as the LEP bounds [12], are found to be compatible with $\nu_h$ assuming the dominance of the $\nu_h$ decay. New limits on mixing $|U_{\mu h}|^2$ obtained by using the recent results on precision measurements of the muon Michel parameters by the TWIST experiment [13] are also found to be consistent with $\nu_h$. Finally, the most stringent bounds on $|U_{\mu h}|^2$ coming from the primordial nucleosynthesis and SN1987A considerations, as well as the limits from the atmospheric neutrino experiments, are also evaded due to the short $\nu_h$ lifetime.

Very recently, the T2K collaboration, which study $\nu_\mu$ neutrino neutrino interactions in a long baseline experiment at J-PARK, has reported on observation of an excess of electron-like events in charge-current quasi-elastic (CCQE) neutrino events over the expected standard neutrino interaction events [14]. A confirmation of the T2K excess and clarification of its origin have great importance for neutrino physics. Although the most popular mechanism for this excess is $\nu_\mu \to \nu_e$ neutrino oscillations with nonzero value of the neutrino mixing angle $\Theta_{13}$, one can still reasonable ask if neutrino oscillations are the only explanation for the T2K result, see e.g [15]. In this work we study a possible manifestation of the presence of $\nu_h$’s in the J-PARC neutrino beam and show that the excess of e-like events observed by T2K could be interpreted as a signal from the production and radiative decay of a $\nu_h$ previously suggested for the explanation of the origin of similar excess events observed by the LSND and MiniBooNe experiments.

In the T2K experiment, specifically designed to search for $\nu_\mu \to \nu_e$ oscillations and for measurements at the first
\( \nu_\mu - \nu_\tau \) oscillation maximum (corresponding to the atmospheric neutrino parameters \( \sin^2 2\theta_{23} = 1 \) and \( \Delta m_{\odot}^2 = 2.4 \times 10^{-3} \text{ eV}^2 \)), the neutrino flux at the far detector location is dominated by \( \nu_\tau \)'s. Therefore, we will assume in the following that the \( \nu_h \) can also be produced in \( \nu_\nu \) NC interactions, e.g. through the mixing with the \( \nu_\tau \) neutrino [16]. Taking into account that the corresponding mixing strength \( |U_{\tau h}|^2 \) is purely constrained by existing experimental data, makes this assumption more interesting. For example, the bounds from the NOMAD experiment \( |U_{\tau h}|^2 \lesssim (4 - 1) \times 10^{-2} \) for the \( \nu_h \) masses from 40 to 80 MeV were obtained from the search for the \( \nu_h \to \nu_\tau e^+ e^- \) decay under assumption that this decay is the principal decay mode of the \( \nu_h \). These limits can be significantly relaxed assuming the dominance of the \( \nu_h \to \gamma \nu \) decay. Direct searches for radiative decays of an excited neutrino \( \nu^* \to \nu \) produced in \( Z \to \nu^* \nu \) decays have also been performed at LEP [10]. For the best limit Br(\( Z \to \nu^* \nu \))Br(\( \nu^* \to \nu \)) / Br(\( Z \to \nu \nu \)) \( \lesssim |U_{\tau h}|^2 \), taking into account \( \) Br(\( Z \to \nu \nu \)) \( \lesssim |U_{\tau h}|^2 \), we find [5]

\[
|U_{\tau h}|^2 \times \frac{m_{\nu_h} [\text{MeV}]}{\tau_{\nu_h} [\text{s}]} < 4.8 \times 10^9. \tag{2}
\]

For the mass and mixing range of (1) it results in \( \tau_{\nu_h} \gtrsim 10^{-11} \text{ s} \).

In addition, there is also a hint from the measurements of the \( D^+_s \to \tau^+ \nu_\tau \) decay rate at CLEO [18, 19]. It has been observed that for some decay modes of outgoing \( \tau \)-leptons, the obtained decay rate of \( D^+_s \to \tau^+ \nu_\tau \) is significantly higher than the predicted one, so that combined branching ratio deviates from the theoretical prediction at the level of \( \gtrsim 10\% \). One may speculate that this inconsistency is due to existence of a sterile neutrino mixed into the tau neutrino. This would result in an additional contribution to the \( D^+_s \to \tau^+ \nu_\tau \) decay rate from the decay \( D^+_s \to \tau^+ \nu_h \). It has been found that for the mass range below 190 MeV the mixing strength required to explain \( D^+_s \to \tau^+ \nu \) discrepancy should be \( |U_{\tau h}|^2 = 0.16 \pm 0.09 \) [2], which for the mass and lifetime range of (1) is consistent with (2) within the large error.

The T2K experiment is described in details in [20]. It uses an almost pure off-axis \( \nu_\mu \) beam originated from the \( \pi^+ \) and \( K \) decays in flight, which are generated by 30 GeV protons from the J-PARC Main Ring accelerator. The detector consists of a near detector complex, used to measure precisely the \( \nu_\mu \) flux and to predict the standard neutrino interaction rate in the far detector, which is the Super-Kamiokande (SK) water Cherenkov detector located at the distance of 295 km from the proton target. The SK detector is a cylindrical tank, about 40 m in diameter and 40 m height, filled with \( \approx 50 \) kt of purified water [21]. The detector has a fiducial volume (FV) of 22.5 kton within its cylindrical inner detector (ID), and a 2 m-wide outer detector (OD) served as a veto against cosmic rays and neutrino interactions in the surrounding rock. The Cherenkov light rings generated by muon, electron and converted photon tracks are used for the reconstruction of the events. The T2K search for e-like events from \( \nu_\mu \to \nu_\tau \) neutrino oscillations uses the data sample collected during the years 2010-2011 [14]. The strategy of the analysis is to identify the \( \nu_\tau \) CCQE candidate events by reconstructing in the FV isolated single e-like rings that are accompanied by no other activity in the outer detector. The measured rate of the e-like events is then compared to the one expected from known reactions. An excess of \( \Delta N = 4.5 \) electron-like events (6 events observed and 1.5\( \pm \)0.3 expected) has been observed in the data accumulated with \( 1.43 \times 10^{20} \) protons on target (pot). For the following discussion several distinctive features of the excess events are of importance [14]: a) the excess is observed for single e-like tracks, originating either from an electron, or from a photon converted into a \( \nu^+ \nu^- \) pair with a typical opening angle \( \approx m_e / E_{e^+e^-} < 1 \) degree (for \( E_{e^+e^-} \gtrsim 100 \text{ MeV} \), which is too small to be resolved into two separate Cherenkov rings in the SK detector; b) the reconstructed neutrino energy is in the range \( 200 < E_{\nu_{\text{vis}}} < 1000 \text{ MeV} \). The variable \( E_{\nu_{\text{vis}}} \) is calculated under the assumption that the observed electron track originates from a \( \nu_\tau \) CCQE interaction; c) the visible energy \( E_{\text{vis}} \) is required to be \( E_{\text{vis}} \gtrsim 100 \text{ MeV} \); d) the angular distribution of the excess events with respect to the incident neutrino direction is wide and consistent with the shape expected from \( \nu_\tau \) CCQE interactions; e) there is no additional significant activity in the OD detector.

To satisfy the criteria a)–e), we propose that the excess events are originated from the production and subsequent radiative decay of a heavy neutrino \( \nu_h \) in the FV of the SK detector. The heavy neutrinos are as-

![FIG. 1: Schematic illustration of the production and subsequent radiative decay of a heavy neutrino in the SK detector (top view). The \( \nu_h \) ’s are produced in \( \nu_\mu \) NC interactions of the J-PARC \( \nu_\mu \) neutrino beam either in the FV, the ID region outside FV, the OD or, as shown, in the surrounding rock. In the later case the \( \nu_h \) would penetrate the rock shield and would be observed in the SK neutrino detector through their \( \nu_h \to \gamma \nu \) decays followed by the decay photon conversion into an e^+e^- pair in the ID FV.](image-url)
assumed to be produced in the neutral-current quasi-elastic (NCQE) interactions $\nu_{\mu}(\tau) + N \rightarrow \nu_h + N$ of muon or tau neutrinos either in the SK FV, the ID region outside FV, OD region, or in the surrounding rock. In the later case, if $\nu_h$ is a relatively long-lived particle, the flux of $\nu_h$’s would penetrate the rock shielding without significant attenuation and would be observed in SK through their $\nu_h \rightarrow \gamma\nu$ decays with the subsequent conversion $\gamma \rightarrow e^+e^-$ of the decay photons in the SK water target, as schematically illustrated in Fig. 2. Similar to $\nu_{\mu} \rightarrow \nu_e$ neutrino oscillations, the occurrence of $\nu_h \rightarrow \gamma\nu$ decays would appear as an excess of single e-like events from decay photon conversion in the SK detector, above those expected from standard neutrino interactions. To make a quantitative estimate, we performed simplified simulations of the $\nu_h$ production and decay processes in the SK discussed above.

The flux of the produced $\nu_h$’s can be calculated by using the following equation for the $\nu_h$ production cross section,

$$\sigma(\nu_{\mu}(\tau)N \rightarrow \nu_hN) \approx \sigma(\nu_{\mu}(\tau)N \rightarrow \nu_{\mu}(\tau)N)|U_{\mu h}|^2 f,$$

where $\sigma(\nu_{\mu}(\tau)N \rightarrow \nu_{\mu}(\tau)N)$ is the cross section for $\nu_{\mu}(\tau)NCQE$ interactions and $f$ is the phase space factor calculated for this two-body reaction, which takes into account dependence on the $\nu_h$ mass. The energy spectra of the produced $\nu_h$’s, whose momenta pointing to the SK fiducial volume, as well as the angular distribution of the $\nu_h$’s, were calculated for different $\nu_h$ masses by taking into account the $\nu_{\mu}, \nu_\tau$ energy distributions at the far detector [14]. In these simulations we used a parametrized $\nu_\nu$ energy spectrum obtained at far detector from the reconstructed $\nu_e$CCQE events [14]. The $\nu_\tau$ energy distribution at the FD position was calculated from the primary $\nu_{\mu}$ spectrum within the standard two-neutrino oscillations scheme for the atmospheric parameters quoted above. The total number of NC events in the FV of the SK detector was used for normalization.

Once the $\nu_h$ flux was known, the next step was to calculate the $e^+e^-$ spectrum based on the $\nu_h \rightarrow \gamma\nu$ decay rate. For a given flux $\Phi_{\nu_h}$, the expected number of signal events from $\nu_h \rightarrow \gamma\nu$ decays occurring within the fiducial length $L$ of the SK detector with the FV entrance point located at a distance $L'$ from the $\nu_h$ production vertex is given by

$$n_{\nu_h} = \sum_{\nu_{\mu},\nu_{\tau}} \int \frac{d\Phi_{\nu_h}}{dE_{\nu_h}d\Omega_{\nu_h}} \frac{m_{\nu_h}}{p_{\nu_h}^2} \frac{\Gamma_{\nu\tau}}{\Gamma_{\nu\nu}} \exp\left(-\frac{L'm_{\nu_h}}{p_{\nu_h}^2\tau_h}\right) \left[1 - \exp\left(-\frac{L'm_{\nu_h}}{p_{\nu_h}^2\tau_h}\right)\right] \frac{\Gamma_{\nu\gamma}}{\Gamma_{\nu\nu}} \frac{\Gamma_{\nu\gamma}}{\Gamma_{\nu\nu}} \Delta R \Delta E \, d\Omega_{\nu_h}$$

where $p_{\nu_h}$ is the $\nu_h$ momentum and $\tau_h$ is its lifetime at the rest frame. $\Gamma_{\gamma\nu}$ and $\Gamma_{\nu\nu}$ are the total and partial mass dependent $\nu_h$-decay widths, respectively. $\varepsilon$ is the $e^+e^-$ pair reconstruction efficiency and the integral is taken over the FV, ID region outside FV, OD and the surrounding rock volume. It is assumed that the total rate $\Gamma_{\tau\nu}$ of the $\nu_{\tau}$ decays is dominated by the radiative decay $\nu_{\tau} \rightarrow \gamma\nu$, i.e. the branching fraction $BR(\nu_{\tau} \rightarrow \gamma\nu) = \frac{\Gamma_{\nu\gamma}}{\Gamma_{\nu\tau}} \approx 1$. The acceptance $A$ of the SK detector was calculated by tracing the produced $\nu_h$’s to the detector FV taking momentum and angular distributions into account. The energy of the photon from the $\nu_h$ decay depends on the initial neutrino energy and on the center-of-mass angle $\Theta$ between the photon momentum and the $\nu_h$ momentum direction. Therefore, the photon laboratory energy spectrum depends on the c.m. angular distribution, which is generally given by $dN/d\cos\Theta = a + b \cos^2\Theta$, where asymmetry coefficient $a$ is in the range $-1 < a < 1$ for Dirac, and $a = 0$ for Majorana neutrinos [22]. The reconstruction efficiency of the photon converted in the fiducial volume of the SK detector was taken to be $\approx 70\%$ from the T2K simulations of the $\nu_e$QECC events [14]. An example of the calculated number of the $\nu_h$ decays in the SK FV is shown in Fig. 2 as a function of the thickness of the rock surrounding the detector for the $\nu_h$ mass of 50 MeV and several $\tau_h$ values. It is seen, that if the $\nu_h$ is a relatively short-lived particle, i.e. $\frac{L'm_{\nu_h}}{p_{\nu_h}^2\tau_h} < 1$ the number of the signal events is quickly saturated and does not depend on the rock thickness. Neutrino interactions, with little hadronic activity in the final state, occurring in the OD or SK support structure, as well as in the part of the ID outside FV, can also yield an isolated e-track from the $\nu_h$ decay in the FV. The attenuation of the $\nu_h$ - flux due to $\nu_h$ interactions in the rock with the average density $3.2\, g/cm^3$ was found to be negligible.

In Fig. 3 an example of distributions of the kinematic
variable $E_{\nu}^{QE}$ for the excess $\nu_h$ decays events in the SK detector reconstructed as $\nu_e$ CCQE events plus neutrino background predicted in Ref. [14] are shown for $E_{vis} > 100$ MeV, $m_{\nu_h} = 50$ MeV, $\tau_{\nu_h} = 10^{-9}$ s, and different values of $a$. These distributions are calculated for the dominant production of $\nu_h$'s by $\nu_e$'s assuming that the $e^+e^-$ pair from the converted photon is mis-reconstructed as a single track from the $\nu_e$ CCQE reaction. The distributions are then normalized to six events, which corresponds $|U_{\tau h}|^2 \simeq 0.025$, to compare them with the T2K data. Simulations are in reasonable agreement with the experimental distributions. For instance, for the distributions shown in Fig. 3 the $\chi^2$ test of their consistency with T2K data yields $p$-values of 0.79, 0.87, and 0.92 for $a = -1$, 0, and $+1$, respectively. In these calculations only statistical errors for both experimental, as reported in Ref. [14], and simulated spectra are included. The test is based on the method of comparison of experimental and simulated histograms recently proposed in Ref. [23], which can be apply for analyzing data samples containing small numbers of events per bin. The simulated excess events, shown in Fig. 3, are mainly distributed in the region $200 \lesssim E_{\nu}^{QE} \lesssim 1200$ MeV. The simulations showed that the shape of the $E_{\nu}^{QE}$ distributions is sensitive to the choice of the $\nu_h$ mass, $\tau_{\nu_h}$, and, in particular, the $a$-parameter values: the smaller the $a$, the softer the spectrum. The distribution of cosine of the opening angle between the $e$-like ring and neutrino beam direction is found to be consistent with $\nu_e$ CCQE events. Taking into account the estimated number of 71 events expected to be observed in the FV from the ordinary NC interactions [14], the total number of $\nu_h$ events inside the fiducial volume of the SK detector is given by $n_{\nu_h} \simeq n_\mu |U_{\mu h}|^2 + n_\tau |U_{\tau h}|^2$, where coefficients $n_\mu, n_\tau$ vary in the range $n_\mu \simeq 12 - 30$ and $n_\tau \simeq 70 - 160$, depending on $\tau_h$. As $|U_{\mu h}|^2 < |U_{\tau h}|^2$ by a factor of a few, mainly $\nu_e$-NC interactions in the FV and in the rock contribute to the total number of excess events. The number of excess events from interactions in the FV is, roughly, $\propto |U_{\tau h}|^2$, while the number of events from the rock is $\propto |U_{\tau h}|^2_{\tau_h}$. In Fig. 4 an example of distribution for the expected number of signal plus neutrino background events is shown in more details in the $(\tau_h; |U_{\tau h}|^2)$ parameter space. For the larger mixing the number of $\nu_h$ events increases, while for smaller lifetime values it decreases due to the more rapid decays of $\nu_h$'s, and mostly NC interactions in the FV contribute in this case. The fraction of excess events expected to be seen in the OD depends on the $\nu_h$ lifetime and typically is $\lesssim 20\%$ ($\lesssim 1$ event) which is consistent with observations [14]. It is also interesting to compare the spatial distributions of the excess events, which, in the case of $\nu_h$ decays, is a combination of the uniform distribution from the NC interactions in the FV and a distribution from NC interactions outside the FV.
From Fig. 2, the number of events from the rock decreases for shorter lifetimes, as one can see from Fig. 2 the number of events from the rock decreases, and mixing values $|U_{\tau h}|^2 \gtrsim 0.03$ are required to keep the signal in the range of 4-5 events. Note, that the increase of $|U_{\tau h}|^2$ results also in increase of the relative fraction of events produced in NC interactions in the FV (typically, about 40% for the long $\tau_h$’s), which are distributed uniformly over the FV.

The probability $P(n_{\nu_h} > 5)$ to observe more than 5 events in the T2K experiment calculated as a function of mixings $|U_{\mu h}|^2$ and $|U_{\tau h}|^2$ is shown in Fig. 5. It was obtained by using the approach of Ref. [24] and taking into account the uncertainties in the background estimate [14]. For example, for $P(n_{\nu_h} > 5) > 0.25$, using [2] to constrain the $\tau_h$, the most suitable values of the parameters are

$$
40 \lesssim m_h \lesssim 80 \text{ MeV}, \quad 10^{-3} \lesssim |U_{\mu h}|^2 \lesssim 10^{-2},
$$

$$
10^{-2} \lesssim |U_{\tau h}|^2 \lesssim 3 \times 10^{-2}, \quad 10^{-10} \lesssim \tau_h \lesssim 10^{-9} \text{ s}. \quad (5)
$$

In summary, in this work we study a possible manifestation of the presence of heavy neutrinos in the J-PARC neutrino beam and show that, assuming the $\nu_h$ mixing into the $\nu_\tau$, the T2K excess events could originate from the same mechanism as those observed by the LSND and MiniBooNE experiments, namely from the production and radiative decay of a sterile neutrino with properties of $\nu_h$. This interpretation is found to be compatible with all the constraints a)-e). The distribution of the excess events in kinematic variable $E_{QE}^\nu$ is found to be consistent with the shapes of distributions obtained within this interpretation. Our analysis may be improved by more accurate and detailed simulations of the T2K experiment, which are beyond the scope of this work. A definite conclusion on the presence of $\nu_h$ events can be drawn when the T2K statistics is substantially increased. Finally, note that several ideas on searching for $\nu_h$ in $\mu$ decays [8], with existing neutrino data [23], in radiative $K$ decays [20, 27], and with neutrino telescopes [28] have been recently proposed. The author thanks D.S. Gorbunov, N.V. Krasnikov and M.E. Shaposhnikov for useful discussions and/or comments, and S.I. Bityukov, A.E. Korneev and D. Sillou for help in calculations.

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