METAL-POOR GLOBULAR CLUSTERS AND GALAXY FORMATION

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ABSTRACT

We demonstrate a significant (\(>5 \sigma\)) correlation between the mean color of metal-poor globular cluster (GC) systems and parent galaxy luminosity. A Bayesian Markov Chain Monte Carlo method is introduced to find the mean color and is easily generalizable to quantify multimodality in other astronomical data sets. We derive a GC color-galaxy luminosity relation of the form \(\langle Z \rangle \propto L^{0.15 \pm 0.03}\). When combined with evidence against a single primordial GC metallicity-galaxy luminosity relation for protogalactic fragments, the existence of such a correlation is evidence against both accretion and major merger scenarios as an explanation of the entire metal-poor GC systems of luminous galaxies. However, our relation arises naturally in an in situ picture of GC formation and is consistent with the truncation of metal-poor GC formation by reionization. A further implication is that the ages of metal-poor GCs in dwarf galaxies constrain the main epoch of galaxy formation in hierarchical models. If the ages of old metal-poor GCs in Local Group dwarfs (\(\geq 11\) Gyr) are typical of those in dwarfs elsewhere, then the bulk of galaxy assembly (at least in clusters and groups) must have occurred at \(z \geq 2.5\), contrary to the predictions of some structure formation models.

Key words: galaxies: formation — galaxies: star clusters

1. INTRODUCTION

A key development in the study of globular clusters (GCs) in external galaxies has been the discovery that most large galaxies have bimodal GC color distributions (e.g., Zepf & Ashman 1993; Forbes, Brodie, & Grillmair 1997; Gebhardt & Kissler-Patig 1999; Kundu & Whitmore 2001a; Larsen et al. 2001). These are usually described as blue (metal-poor) and red (metal-rich) GC subpopulations, although additional substructure may be present. The red GC system properties appear to be intimately tied to those of their parent galaxy, suggesting that the red GCs formed along with the bulk of the galaxy field stars (Forbes et al. 1997; Forbes & Forte 2001; Larsen et al. 2001). In both spiral and elliptical galaxies, they are thought to be associated with the bulge/spheroid component (Forbes, Brodie, & Larsen 2001).

The blue GCs are among the oldest and most metal-poor stellar systems observable. Therefore, they provide a probe of very early epochs of star formation in the universe. Whether or not the properties of blue GCs correlate with the mass of their parent galaxy has been controversial (Forbes et al. 1997; Côte et al. 2000; Burgarella, Kissler-Patig, & Buat 2001; Forbes & Forte 2001; Larsen et al. 2001; Lotz 2003; Lotz et al. 2004), and no clear demonstration of such a relation exists in the literature. However, the issue is an important one in the context of GC and galaxy formation. If a correlation exists, it implies that the blue GCs, or at least a significant proportion of them, “knew” about the galaxy to which they would ultimately belong. This indicates that their formation was affected by the local conditions, and that they may have already been contained within the dark matter halo of their final galaxy. The detailed chemical and age structure within the blue GC systems of galaxies of various types and environments would then offer one of the few observational constraints on the properties of the protogalactic clouds that combined to build the galaxies that we observe today. Such a correlation would also rule out any formation mechanism whereby all metal-poor GCs form completely independently of a host galaxy (e.g., Peebles & Dicke 1968).

Our aim here is to consider galaxies over a large luminosity range, use only high-quality data, and analyze the photometry in a uniform manner. In this way, we will reduce the random and systematic errors that could disguise the existence of a blue GC–host galaxy correlation. In particular, we have added new data on the GC systems of dwarf and low-luminosity elliptical galaxies and used a Bayesian statistical method to find the peak of the blue GC color distribution.

2. SAMPLE AND METHOD

We chose to explore a possible correlation between the mean \(V-I\) color (i.e., the mode/peak of the Gaussian distribution) of metal-poor GC systems and the \(M_V\) of their host galaxies, since most GC system studies have been carried out in the \(V\) and \(I\) bands. When using only optical colors the age-metallicity degeneracy is always a concern, but recent spectroscopic results suggest that, despite the presence of a small fraction of intermediate-age GCs in some early-type galaxies (Goudfrooij et al. 2001; Larsen et al. 2003; Strader et al. 2003b), both metal-poor and metal-rich GC subpopulations appear to be very old (\(\geq 10\) Gyr) within model uncertainties (e.g., Larsen et al. 2002; Larsen & Brodie 2002).

Our sources for massive early-type galaxies were Larsen et al. (2001) and Kundu & Whitmore (2001a, 2001b), who determined the peaks of the blue and red GC subpopulations by fitting Gaussians as part of the KMM routine (Ashman, Bird, & Zepf 1994). In addition, several nearby luminous spiral galaxies have enough blue GCs to have their mean colors

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accurately determined. These include the Milky Way and M31
(Harris 1996; Barmby et al. 2000), as well as several Sculptor
Group galaxies (Olsen et al. 2004). Our method (see below)
uses photometry for individual GCs, and we derive the peaks
and errors ourselves rather than just using those reported in
the literature. Therefore, only galaxies with high-quality Hubble
Space Telescope (HST) data (which has minimal contamination)
and for which we had access to the photometry are included.

To probe the metal-poor GC systems of low-luminosity
galaxies, we also included Local Group dwarf galaxies in our
sample. These were primarily taken from the compilation of
Forbes et al. (2000), although we have used new spectroscopic
metallicities for old LMC GCs (Beasley, Hoyle, & Sharples
2002) whenever possible. The metallicities of Fornax GCs
were taken from the study in Strader et al. (2003a), and we
have added NGC 4147 to the metal-poor Sagittarius dwarf
GCs (Bellazzini et al. 2003). The Local Group sample was
supplemented with the M81 dwarf DDO 78, which has one
GC (Sharina, Sil’chenko, & Burenkov 2003). Most of the
dwarf GCs have spectroscopic and/or color-magnitude dia-
gram (CMD) based metallicities (presumably superior to those
obtained from their V−I colors), and these were converted
into V−I colors using the Galactic relation of Barmby et al.
(2000). We included only genuinely old GCs, excluding, for
example, intermediate-age GCs in the Magellanic Clouds.
While further detections of GCs in dwarf galaxies outside the
Local Group have been claimed (e.g., in the M81 group;
Karachentsev et al. 2000), we included only those whose
identities have been confirmed by spectroscopy. Finally, we
note that since the majority of our sample galaxies are in
groups or clusters, at present we can only claim to be ex-
ploring the existence of a correlation in these environments.

For all galaxies with four or more GCs, we used Bayesian
Markov Chain Monte Carlo (MCMC) methods, implemented
in the package WinBUGS (Spiegelhalter et al. 2003), to find
the mean color of the blue GCs. See Gilks, Richardson, &
Spiegelhalter (1996) and Strader & Brodie (2004) for more
details on MCMC methods and for comparisons to classical
methods, e.g., maximum likelihood. For the luminous early-
type galaxies, as well as the Milky Way and M31, we fitted a
homoscedastic (equal variance) Gaussian mixture model to the
V−I colors to estimate the values of the blue and red peaks,
as well as credible posterior intervals (the Bayesian equivalent
of confidence intervals) around those values. Indeed, the accurate
estimation of these posterior intervals is one of the main
advantages of using Bayesian method over the standard least-
squares framework. In the remainder of the galaxies, which
had at most 18 blue GCs, a single Gaussian was fitted only
to the metal-poor GCs (taken to be those with [Fe/H] < −1).
For galaxies with fewer than four GCs, the mean of the indi-
vidual V−I colors was used, with a fixed 0.05 mag (equivalent
to ∼0.3 dex) 1σ error as a conservative estimate of the ac-
tual error.

Using WinBUGS, we fitted a hierarchical linear model to the
galaxy absolute magnitudes and mean GC colors. We made
the a priori choice of a linear model because such models in
(M_{V_{I}}, V−I) observational space reflect power-law models in
luminosity/metallicity (L, Z) theoretical space. Our model has
the following form:

\begin{align}
V−I_{\text{est}} &= \alpha + \beta M_{V_{I}}; \\
V−I_{\text{cosmic}} &\sim N(V−I_{\text{est}}, \sigma_{\text{cosmic}}^{2}), \\
V−I &\sim N(V−I_{\text{cosmic}}, \sigma_{I}^{2}).
\end{align}

Diffuse (noninformative) priors were placed upon \(\alpha, \beta, \) and
\(\sigma_{\text{cosmic}}^{2} \). \(V−I_{\text{est}}\) is the initial estimated blue peak for the 4th
galaxy given the priors on \(\alpha\) and \(\beta\). Cosmic variance and
measurement errors are then hierarchically propagated to
model the observed blue peak \(V−I\) for each galaxy.

3. RESULTS AND ERROR ANALYSIS

3.1. Results

The resulting best-fit weighted model is \(V−I = (-0.0091 \pm 0.0018)M_{V_{I}} + (0.74 \pm 0.04)\), which is significant
at the 5σ level. An unweighted model \(V−I = (-0.010 \pm
0.0015)M_{V_{I}} + (0.72 \pm 0.03)\) has a nearly identical slope at an
even higher level of significance ( > 6σ). This suggests no
significant bias is introduced by our calculated errors, and that
the slope of the weighted model is not being defined by a
small number of luminous galaxies with very accurately mea-
sured peaks. The nonparametric Spearman rank correlation
test confirms the correlation between \(M_{V_{I}}\) and mean \(V−I\) for
blue GCs without assuming a specific model, finding a
probability \(p \leq 4.8 \times 10^{-7}\) that there is no monotonic rela-
tion between the two variables. We also separately fitted
weighted and unweighted models to only the spheroidal
galaxies in our sample (42 of the total 53 galaxies), since the
younger stellar populations in disk galaxies may complicate
our use of \(M_{V_{I}}\) as a tracer of galaxy mass. The resulting
models are \(V−I = (-0.0085 \pm 0.0019)M_{V_{I}} + (0.76 \pm 0.04)\)
and \(V−I = (-0.011 \pm 0.0015)M_{V_{I}} + (0.71 \pm 0.03)\), respec-
tively, and very similar to those for the full sample.

The “universal” slope of roughly −0.01 found above is
consistent at the ∼1σ level with the results of Larsen et al.
(2001), −0.016 ± 0.005, and of Burgarella et al. (2001),
−0.009 ± 0.002. The bottom part of Figure 1 shows mean
\(V−I\) color for metal-poor GCs versus parent galaxy \(M_{V_{I}}\).

While there are not enough disk galaxies to meaningfully
derive a slope for these galaxies alone, an examination of
Figure 1 suggests that they may have systematically bluer
metal-poor GC systems than spheroid-dominated galaxies: all
eight disk galaxies with \(M_{V_{I}} < −18\) fall below the best-fit
model line for the full sample. The apparent offset at \(M_{V_{I}} =
−20\) is ∼−0.02 mag, equivalent to just over ∼0.1 dex in met-
ality. This difference is likely partially due to our use of \(M_{V_{I}}\)
as a tracer for galaxy mass, but an interpretation with a simple
closed-box chemical evolution model also suggests that, at
fixed luminosity, disk galaxies had a larger gas fraction than
spheroidal galaxies at the time their metal-poor GCs formed.
This, in turn, implies that either (1) metal-poor GCs in disk
galaxies are older than their spheroidal counterparts, or (2)
an initial phase of chemical enrichment (to ∼0.03–0.05 \(Z_{\odot}\))
proceeded more quickly in elliptical than in spiral galaxies.

For comparison to theoretical predictions, it may be helpful
to express our relation \(L \propto I^{m}\) form. Using the Galactic color-
metallicity relation \(V−I = (0.156 \pm 0.015)[Fe/H] + (1.15 \pm
0.02)\) (Barmby et al. 2000), we find \(Z \propto I^{0.15±0.03}.\)

3.2. Error Analysis

Could systematic statistical biases be responsible for our
relation? First, we note that many of the possible sources of

\footnote{In Fig. 1, absolute magnitudes for luminous early-type galaxies were taken
from Prugniel & Simien (1996), while Local Group galaxies came from Pritchet
& van den Bergh (1999). For Sculptor Group galaxies, the distance moduli
were from Karachentsev et al. (2003), with photometry from Fitzgibbons
(1990), Pierce & Tully (1992), and de Vaucouleurs et al. (1991). All Galactic
reddening corrections were from Schlegel, Finkbeiner, & Davis (1998).}
the colors of the subpopulations themselves (e.g., Lee, Kim, & Geisler 1998; Harris, Harris, & McLaughlin 1998). Thus, it does not appear likely that selection effects could have produced our relation.

Point 2 above posits that our observed correlation is an artifact of the assumptions used to estimate the color distributions, namely, that the observed distributions can be well-described as a superposition of two Gaussians with equal variance. Criticisms could be made of the assumptions of (1) bimodality, (2) Gaussian distributions, or (3) homoscedasticity. Since galaxies in this subsample were selected to be visually bimodal, as well as generally exhibiting strong statistical evidence against unimodality (see Larsen et al. 2001), arguing against the assumption of bimodality requires instead that three or more subpopulations of GCs are present in the majority of the galaxies. No convincing demonstrations of such multimodal systems have been made, even though some galaxies now have very deep HST data (e.g., M87; Jordán et al. 2002). Assumption 2 can be motivated a priori by the lognormal metallicity distributions predicted by a simple closed-box chemical evolution model, appealing to the Central Limit Theorem, or to the dominance of Gaussian photometric errors. It could be argued that GC color distributions could have heavier tails than Gaussians and be better fitted by, e.g., Student’s t distributions (as the Galactic GC luminosity function appears to be; Secker 1992). As a test of this hypothesis, we fitted the GC colors of M87 with a model very similar to that in § 2, except that we used t distributions (instead of Gaussians) with the degrees of freedom as a free parameter. The posterior distributions of this parameter had most of their mass at large values, suggesting that Gaussian fits are indeed appropriate (since a t tends to a Gaussian as the degrees of freedom tend to infinity).

Regarding assumption 3 of homoscedasticity, due to the degeneracy between variance and other parameters in mixture model fits, it is generally desirable assume a homoscedastic model unless there is a priori evidence against it (e.g., Ashman et al. 1994). For our sample, the blue and red GCs have similar luminosity functions (e.g., Larsen et al. 2001), so photometric errors could not be the source of unequal variances. Thus, any differences would have to be intrinsic. The Galactic GC system, the only one that has metallicities measured for nearly all clusters, appears to be homoscedastic within measurement errors (Côté 1999). In addition, any proposed heteroscedasticity would need to be finely tuned, with an ever larger fraction of metal-rich GCs “wrongly” assigned to the metal-poor peak with increasing galaxy luminosity, to have any prospect of producing our relation. As a simple numerical example, assume that all galaxies have a “base” mean blue GC color of $V-I = 0.90$. Our relation indicates that the most luminous galaxies in our sample have blue GC colors $V-I = 0.95$ and red GC colors $V-I = 1.20$. Since the final peak is essentially a number-weighted average of the individual GC colors, and such galaxies have similar numbers of blue and red clusters, an unreasonable $\pm 25\%$ of the red GCs would have to be regularly misassigned to the blue peak to produce the colors we see for such galaxies (this is in addition to the ad hoc nature of the tuning noted above).

In summary, we find no evidence that systematic statistical biases could have led to the observed correlation between mean metal-poor GC color and parent galaxy luminosity.

4. IMPLICATIONS AND DISCUSSION

The classic Fall & Rees (1988) classification of GC formation scenarios into primary, secondary, and tertiary has in
the last decade given way to a new triad: accretion (e.g., Côté, Marzke, & West 1998), major merger (e.g., Ashman & Zepf 1992), and in situ (e.g., Forbes et al. 1997). The primary focus of each of these formation scenarios is the GC systems of giant ellipticals (gE’s). However, much of the following discussion applies also to the formation of less luminous ellipticals (E’s) and disk galaxies.

Côté et al. (1998, 2000, 2002) were able to produce bimodal metallicity distributions for the GC systems of luminous galaxies under the fundamental assumption that all galaxies have one intrinsic population of GCs, which depends on galaxy luminosity. They used observations of a sample of dwarf and giant galaxies to find a “primordial” relation between GC metallicity and parent galaxy luminosity. By varying an assumed mass spectrum of protogalactic fragments, they were able to produce a wide variety of GC metallicity distributions, some of which matched the bimodal form seen in most giant galaxies. It should be noted that they assume dwarf galaxies in the local universe (and especially in the Local Group) are the surviving counterparts of these protogalactic fragments. If instead these gaseous fragments merged themselves out of existence at roughly the epoch of blue GC formation, then the model is essentially equivalent to an in situ scenario (see below).

The Côté et al. (2002) primordial mean metallicity–$M_V$ relation (see their Fig. 1) is $V-I = -0.055 M_V + 0.04$. This relation predicts that galaxies with $M_V = -17.5$ will have one intrinsic population of GCs with $V-I = 1.00$. By contrast, the blue GC relation we derived above and the red GC relation from Larsen et al. (2001) predict peaks at $V-I = 0.90$ and $V-I = 1.09$, respectively. In Figure 1, we have overplotted red GC peaks for 15 galaxies from Larsen et al. (2001). To these we have added four less-luminous galaxies (which are in our blue sample as well) for which we have remeasured the red peaks ourselves, using original data from Larsen et al. and Kundu & Whitmore (2001a, 2001b). The dotted line is a new linear fit to the red peaks, weighted by the number of GCs in each peak. The dashed line is the Côté et al. relation. While the observations are marginally consistent with the primordial relation at the blue and red ends of the luminosity range, in the intermediate-metallicity region between $M_V = -17$ and $-18$ there is a clear, ~0.1 mag difference between the observed peaks and the primordial prediction. Thus, the Côté et al. primordial relation for a single intrinsic population of GCs appears to be less consistent with current observations than the existence of two separate (blue and red) GC metallicity–luminosity relations.

Côté et al. (2002) showed that by using their primordial relation, a wide variety of GC color distributions could be produced. An examination of their Figure 1 suggests that, given appropriate input assumptions, the accretion model could reproduce the blue GC relation. However, the ability of the accretion model to successfully reproduce our observed relation is critically dependent on the validity of the primordial relation. By contrast, a metal-poor GC-galaxy luminosity correlation arises naturally under in situ scenarios for GC formation, e.g., Harris & Pudritz (1994) and Forbes et al. (1997). In such scenarios, enrichment of the interstellar medium is linked to the depth of the galactic potential, independent of the details of GC formation in a particular scenario.

A blue GC-galaxy relation places limits on the degree to which an intrinsic population of metal-poor GCs in a luminous galaxy has been affected by accretion and/or mergers, with substantial implications for galaxy formation models (see below). A caveat is that the cosmic variance in our model (1 $\sigma$ scatter of ~0.02 mag) does not rule out the formation of the metal-poor GC systems of gE’s like M49 and M87 from the accretion of several slightly less luminous galaxies with redder-than-average blue GCs. However, our correlation implies that in the mean the blue GC systems of gE’s could not have formed primarily from the accretion of less luminous galaxies, especially $M_V > -18$ dwarfs, whose blue GCs have mean $V-I \leq 0.90$. The paucity of metal-poor field stars in the halos of luminous E galaxies (e.g., NGC 5128; Harris & Brodie 2000) is another argument against significant accretion, since such stars would presumably accompany the accreted metal-poor GCs (Harris 2003). We are not arguing that accretion does not take place; witness the existence of the Sagittarius dwarf (Ibata, Gilmore, & Irwin 1994), the recently discovered Canis Major galaxy (Martin et al. 2004; Forbes, Strader, & Brodie 2004), relic stellar streams in the halo of M31 (Ibata et al. 2001), and more distant systems (e.g., Forbes et al. 2003). However, we do suggest that it is not the primary mechanism by which the GC systems of most luminous galaxies are built.

We note that a major merger scenario for the formation of gE’s is also difficult to reconcile with our results, since the mean colors of metal-poor GCs in typical Sb/Sc spirals like the Milky Way and M31 are bluer than those of gE’s (see Fig. 1). The favored site for the formation of blue GCs in the major merger scenario is in pregalactic fragments (Ashman & Zepf 1992). Ashman (2003) states “some variation in mean metallicity [of metal-poor GCs] would not rule out this option provided it did not correlate with properties of the current parent galaxy.” As noted above for the accretion model, while cosmic variance would allow the occasional merger of two $L_*$ spirals with redder-than-average blue GCs, the existence of a global correlation suggests that major mergers are unlikely to be the dominant mechanism for the creation of the GC systems of gE’s. Independent arguments in favor of this point have been made based upon the relative numbers of metal-poor GCs in spirals and gE’s (see Harris 2003 for a summary), although some recent work (e.g., Rhode & Zepf 2004) suggests that these “specific frequency” arguments may only pose a problem for the blue GC systems of gE’s. We note that proponents of the merger scenario have themselves argued (see, e.g., the discussion in Ashman & Zepf 1998) that major mergers cannot be the exclusive mechanism for forming gE’s.

In situ scenarios have been criticized with straw man comparisons to monolithic collapse models (e.g., Eggen, Lynden-Bell, & Sandage 1962), although, for example, Forbes et al. (1997) argued that the initial collapse probably involved “some chaotic merging of many small subunits” as in the Galactic formation model of Searle & Zinn (1978). This idea was reflected in simulations of GC formation by Beasley et al. (2002). One of the most significant problems with the in situ scenario is the lack of a definitive physical mechanism for the truncation of metal-poor GC formation. An initial starburst, accompanied by the formation of metal-poor GCs, could conceivably ionize and/or remove a substantial mass of gas from inner regions of the protogalaxy, with the subsequent infall of enriched gas forming a population of metal-rich GCs and the bulk of the galaxy starlight (Forbes et al. 1997). However, this feedback mechanism would be increasingly ineffective in more massive halos, with little suppression of star formation expected for halos with virial velocities $V > 100$ km s$^{-1}$ (Dekel & Woo 2003). Thus, feedback is unlikely to be the source of the near-universal metallicity gap observed in the GC systems of massive galaxies with $V$ roughly several
hundred kilometers per second. Cosmic reionization might also result in a rapid truncation of blue GC formation (e.g., Santos 2003), although some instead argue for reionization as the trigger for metal-poor GC formation (Cen 2001). Among the advantages of the reionization hypothesis are its consistency with early structure formation theories, as well as the prediction of the observed differences in metal-poor GC specific frequency between elliptical and spiral galaxies. Since elliptical galaxies (located in high-density peaks) collapse earlier than spirals of similar mass, they have a larger fraction of their final mass assembled and available for GC formation before reionization. By a similar argument, one might expect the metal-poor GC metallicity–galaxy luminosity relation to have a steeper slope in denser environments. A study comparing the blue GC systems of field and cluster galaxies might then offer the intriguing possibility of elucidating the relative roles of galaxy mass and environment in shaping the initial phase of local metal enrichment.

Our findings also have implications for popular hierarchical structure formation models (e.g., Kauffmann, White, & Guiderdoni 1993; Cole et al. 2000; Somerville, Primack, & Faber 2001). For example, semianalytic models generically predict a substantial fraction of mass assembly at $z \approx 5$. However, as already noted, relatively luminous E’s cannot have accreted very many dwarf galaxies and their populations of GCs, since this would destroy our observed correlation. The ages of metal-poor GCs in dwarf galaxies place lower limits on the possible epochs of significant accretion. We note that our results do not constrain (1) the accretion of galaxies before the formation of their GC systems, (2) the accretion of galaxies without GCs (which typically have $M_r > -13$), or (3) the formation of field galaxies. However, if the ages of old metal-poor GCs in Local Group dwarfs ($\geq 11$ Gyr; Johnson et al. 1999) are typical of those elsewhere (an untested assumption), then the bulk of galaxy assembly in groups and clusters must have occurred at $z \approx 2.5$. For more likely mean GC ages of $\sim 12$ Gyr, the primary epoch of mass assembly is pushed to $z \sim 4$ or higher.

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Spiegelhalter, D., Thomas, A., Best, N., & Lunn, D., 2003, WinBUGS User Manual (Cambridge: MRC BSU)

Strader, J., & Brodie, J. P. 2004, in preparation

Strader, J., Brodie, J. P., Forbes, D. A., Beasley, M. A., & Huchra, J. P. 2003a, AJ, 125, 1291

van den Bergh, S. 1996, AJ, 112, 2634

Zepf, S. E., & Ashman, K. M. 1993, MNRAS, 264, 611