Overview of Electroweak Baryogenesis

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Electroweak baryogenesis is briefly overviewed with emphasis on nondecoupling loop properties of the scalar particles. In particular, quantum corrections to the triple Higgs boson coupling is discussed as a probe of electroweak baryogenesis.

I. INTRODUCTION

According to the cosmological data, the baryon asymmetry of the universe (BAU) is found to be

\[ \eta_{\text{CMB}} = \frac{n_b}{n_\gamma} = (6.23 \pm 0.17) \times 10^{-10}, \quad (1) \]

\[ \eta_{\text{BBN}} = \frac{n_b}{n_\gamma} = (5.1 - 6.5) \times 10^{-10}, \quad (95\% \, \text{C.L.}). \quad (2) \]

Clarification of the origin of the BAU is one of the greatest challenges in particle physics and cosmology. If the BAU is generated before \( T = \mathcal{O}(1) \) MeV, the light element abundances (D,\(^3\)He,\(^4\)He,\(^7\)Li) can be explained by the standard Big-Bang cosmology. To get the right \( \eta \) (which is called baryogenesis) from an initially baryon symmetric universe, the so-called Sakharov’s conditions should be satisfied \( [2] \): (i) baryon number \( (B) \) violation, (ii) C and CP violation, (iii) departure from thermal equilibrium. To this end, a lot of scenarios have been proposed so far \( [3] \). From an experimental point of view, electroweak baryogenesis (EWBG) \( [4] \) among others is the most testable scenario, and thus it is in urgent need of detailed analysis in the LHC and future ILC eras. Since it is not very trivial to satisfy all the Sakharov’s conditions within the EWBG framework, some distinctive features are required in the feasible region and thus may yield striking signals to the low energy observables.

In this talk, the EWBG is reviewed focusing especially on nondecoupling loop properties of scalar particles that may help for realizing the strong first-order phase transition (EWPT). As a consequence of the nondecoupling scalar loop, quantum corrections to the triple Higgs boson coupling is discussed.

II. EWBG MECHANISM

Foregoing Sakharov’s conditions in the EWBG are satisfied as follows: (i) \( B \) violation is realized by an anomalous process at finite temperature (conventionally referred as sphaleron process although the sphaleron solution does not exist in the symmetric phase.) (ii) C is maximally violated by the chiral gauge interactions, CP violation comes from the Cabbibo-Kobayashi-Maskawa matrix \( [5] \) or other complex parameters once the standard model (SM) is extended. (iii) Out of equilibrium is realized by the first-order EWPT with bubble nucleation and expansion.

The left panel of Fig. 1 shows a schematic picture of the expanding bubble wall. The inside of the bubble corresponds to the broken phase where the Higgs vacuum expectation value (VEV) is nonzero, \( \langle \Phi \rangle \neq 0 \) while the outside of it represents the symmetric phase where \( \langle \Phi \rangle = 0 \). In the right panel of Fig. 1, \( \langle \Phi \rangle \) is depicted as a function of \( z \) which is a direction of the bubble expansion. The outline of the EWBG is as follows.

1. Because of \( CP \) violation induced by interactions between the bubble and the particles in the plasma, chiral charges are asymmetric.

2. They diffuse into the symmetric phase and accumulate.

3. \( B \) is generated via sphaleron process.

4. After decoupling of the sphaleron process in the broken phase, \( B \) is fixed.

The last step may leave a detectable footprint in low energy observables. In the following, we will look into one of such possibilities.
III. SPHALERON DECOUPLING CONDITION

In order to preserve the generated BAU via the sphaleron process in the symmetric phase, the $B$-changing rate in the broken phase ($\Gamma_B^{(b)}$) must be sufficiently suppressed. Namely,

$$\Gamma_B^{(b)}(T) \simeq \text{(prefactor)} e^{-E_{\text{ph}}(T)/T} < H(T) \simeq 1.66 \sqrt{g_*(T) T^2/m_P}$$

is satisfied, where $E_{\text{ph}}$ denotes the sphaleron energy, $g_*$ is the degrees of freedom of relativistic particles in the plasma ($g_* = 106.75$ in the SM) and $m_P$ stands for the Planck mass which is about $1.22 \times 10^{19}$ GeV. Since $E_{\text{ph}}$ is proportional to the Higgs VEV (denoted by $v$), Eq. (3) can be realized if the EWPT is strongly first-order.

Conventionally, the sphaleron energy is parametrized as $E_{\text{ph}}(T) = 4\pi v(T)E(T)/g_2$, where $g_2$ denotes the SU(2) gauge coupling constant. Eq. (3) is then cast into the form

$$\frac{v(T)}{T} > \frac{g_2}{4\pi E(T)} \left[42.97 + \text{log corrections}\right].$$

The dominant contributions on the right-hand side is $E(T)$ while the log corrections that mostly come from the zero mode factors of the fluctuations about the sphaleron typically amount to about 10% [6].

As an illustration, we evaluate the sphaleron energy at zero temperature, $E(0)$, within the SM [7]. Since the $U(1)_Y$ contribution is sufficiently small [8], it is enough to confine ourself to the SU(2)$_L$ gauge-Higgs system. To find the sphaleron solution, we adopt a spherically symmetric configurations ansatz with a noncontractible loop [7].

In Fig. 2, $E(0)$ is plotted as a function of $\lambda/g_2^2$. We can see that as $\lambda/g_2^2$ increases, $E$ increases. For the Higgs boson with a mass of 126 GeV, which corresponds to $\lambda \simeq 0.13$, one finds $E(0) \simeq 1.92$. With this value, Eq. (4) becomes

$$\frac{v(T)}{T} > 1.16,$$  

where only the dominant contributions are retained on the right-hand side in Eq. (4). Note that the use of $E(0)$ in the decoupling criterion leads to somewhat underestimated results since $E(T) < E(0)$. In the MSSM, using the finite-temperature effective potential at the one-loop level, $v(T_N)/T_N > 1.38$ is obtained, where the sphaleron energy as well as the translational and rotational zero mode factors of the fluctuation around the sphaleron are evaluated at a nucleation temperature ($T_N$) which is somewhat below $T_C$ [6].

From the argument here, the degree to which the first-order EWPT is strengthen is one of the central questions to be answered for successful baryogenesis. There are several ways to achieve the strong first-order EWPT (see a recent study [9]). In what follows, we will focus on the thermally driven case, specifically.

Since most of collider probes of the EWBG are intimately related to the sphaleron decoupling condition, the reduction of theoretical uncertainties in this condition is indispensable for reaching the definitive conclusion of viability of the EWBG. So far, a high-temperature expansion has been exclusively used to evaluate the sunset diagrams in the two-loop analysis of the EWPT. Recently, the validity of such a high-temperature expansion is investigated in the Abelian-Higgs and its extended models in [10]. For gauge dependence issues in the perturbative analysis of the EWPT, see e.g. [11-13] and references therein.
IV. ELECTROWEAK PHASE TRANSITION

Here, we explicitly demonstrate why the SM EWBG fails, which may give a signpost searching for new physics. Using a high-temperature expansion, the one-loop effective potential at finite temperature is reduced to

\[ V_{\text{eff}}(\varphi; T) \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4} \varphi^4, \]

where

\[ D = \frac{1}{8v^2} \left( 2m_W^2 + m_Z^2 + 2m_t^2 \right), \quad E = \frac{1}{4\pi v^3} \left( 2m_W^3 + m_Z^3 \right) \simeq 10^{-2}, \]

\[ \lambda_T = \frac{m_h^2}{2v^2} \left[ 1 - \frac{3}{8\pi^2} \frac{m_W^2}{m_h^2} \left\{ 2m_W^4 \log \frac{m_W^2}{\alpha_B T^2} + m_Z^2 \log \frac{m_Z^2}{\alpha_B T^2} - 4m_t^4 \log \frac{m_t^2}{\alpha_F T^2} \right\} \right], \]

with \( \alpha_B = 2 \log 4\pi - 2 \gamma_E \simeq 3.91 \) and \( \alpha_F = 2 \log \pi - 2 \gamma_E \simeq 1.14 \). Appearance of the cubic term with the negative coefficient dictates that the EWPT should be first-order. Note that since the origin of the cubic term is the zero Matsubara frequency mode, the only bosonic thermal loops contribute to \( E \).

The critical temperature \( T_C \) is defined by a temperature at which \( V_{\text{eff}}(\varphi; T) \) has two degenerate minima. At \( T_C \), \( V_{\text{eff}} \) takes the form

\[ V_{\text{eff}}(\varphi; T_C) = \frac{\lambda_{T_C}}{4} \varphi^2 (\varphi - v_C)^2, \quad v_C = \frac{2ET_C}{\lambda_{T_C}}. \]

As we discussed in the previous section, \( v_C/T_C \gtrsim 1 \) should hold to avoid the washout by the sphaleron in the broken phase. Since \( \lambda_{T_C} \simeq m_h^2/2v^2 \), one obtains the upper bound of the Higgs boson mass as

\[ m_h \lesssim 2v\sqrt{E} \simeq 48 \text{ GeV}. \]

This mass range has been already excluded by the LEP experiments. According to nonperturbative studies, the EWPT in the SM is a crossover for \( m_h \gtrsim 73 \text{ GeV} \) [14].

From the above argument, one of the straightforward way-outs is to enhance \( E \) by adding the bosonic degrees of freedom. However, in the case of scalar particle, the degree to which \( E \) is enhanced highly depends on the loop properties, namely, \textit{decoupling} or \textit{nondecoupling}.

Suppose a mass of a scalar is given by

\[ m^2 = M^2 + \tilde{\lambda}\varphi^2, \]

where \( M \) is a mass parameter in the Lagrangian or a thermally corrected mass at finite temperature, and \( \tilde{\lambda} \) is a coupling constant between the Higgs boson and the scalar. Depending on the magnitudes of \( M \) and \( \tilde{\lambda} \), two cases are conceivable:

\[ V_{\text{eff}} \owns \begin{cases} -\frac{\tilde{\lambda}^3}{2T} \varphi^3 \left( 1 + \frac{M^2}{\tilde{\lambda}\varphi^2} \right)^{3/2}, & \text{for } M^2 \ll \tilde{\lambda}\varphi^2, \\ -|M|^3T \left( 1 + \frac{\tilde{\lambda}\varphi^2}{M^2} \right)^{3/2}, & \text{for } M^2 \gtrsim \tilde{\lambda}\varphi^2. \end{cases} \]
Note that the first case (what we call nondecoupling [27]) can generate the cubic-like term so the $E$ is enhanced while the latter (decoupling) does not. This is the reason why the Higgs boson whose mass is given by $m_h^2(\varphi) = -m_h^2/2 + 3\lambda\varphi^2$ does not contribute to $E$ significantly.

In summary, what one needs for realizing the strong first-order EWPT via the thermally driven mechanism are (1) relatively large coupling constant $\lambda$ and (2) small mass parameter $M$ [28]. Phenomenological implications of such a nondecoupling scalar are discussed below.

V. TRIPLE HIGGS BOSON COUPLING AS A PROBE OF EWBG

As an interesting consequence of the strong first-order EWPT, we consider quantum corrections to the triple Higgs boson coupling. Here, we take the two Higgs doublet model (2HDM) as an illustration [17]. We impose a $Z_2$ symmetry to avoid Higgs-mediated flavor changing neutral current processes at the tree level. In the Higgs potential, however, such a discrete symmetry is softly broken by $\Phi^\dagger Z \beta$ while the latter (decoupling) does not. This is the reason why the Higgs boson whose mass is given by $m_h$.

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In summary, what one needs for realizing the strong first-order EWPT via the thermally driven mechanism are (1) relatively large coupling constant $\lambda$ and (2) small mass parameter $M$ [28]. Phenomenological implications of such a nondecoupling scalar are discussed below.
In such a case, $\Delta \lambda_{h hh}^{2\text{HDM}}/\lambda_{h hh}^{\text{SM}}$ would be larger than 10%. Remarkably, if the heavy Higgs bosons have strong nondecoupling loop effects, $\Delta \lambda_{h hh}^{2\text{HDM}}/\lambda_{h hh}^{\text{SM}}$ can reach 100%. Note that it does not necessarily imply the breakdown of perturbation since the Higgs quartic couplings appearing in the tree-level $\lambda_{h hh}$ and those in the one-loop expression are essentially different in a sense that the combinations of $\lambda_{1-5}$ are different. Actually, $\lambda_{1-5} < 4\pi$ are still maintained.

Let us consider the MSSM case next. The EWBG scenario in this model is the so-called “light stop scenario (LSS)” [17], which is now on the verge of being excluded. (see e.g. [18] [19].

In order to realize the physical Higgs boson mass, the left-handed stop SUSY breaking mass ($m_{\tilde{q}}$) has to be much greater than the right-handed one ($m_{\tilde{t}_R}$). According to [19], $m_{\tilde{q}}$ may be as large as $\mathcal{O}(10^9)$ TeV. In such a case, the effective theory approach is more appropriate. The effective theory of the LSS is constructed in [20] and is applied to the EWBG [19] [21]. Here, to make our analysis simple, we take $m_{h}$ as an input.

In the limit of $m_{\tilde{q}} > m_{\tilde{t}_R}$, the stop masses are reduced to

$$
\bar{m}_{\tilde{t}_2}^2 = m_{\tilde{q}}^2 + \frac{y_t^2 \sin^2 \beta}{2} \left( 1 + \frac{|X_t|^2}{m_{\tilde{q}}^2} \right) \varphi^2 + \mathcal{O}(g^2) \simeq m_{\tilde{q}}^2,
$$

$$
\bar{m}_{\tilde{t}_1}^2 = m_{\tilde{t}_R}^2 + \frac{y_t^2 \sin^2 \beta}{2} \left( 1 - \frac{|X_t|^2}{m_{\tilde{q}}^2} \right) \varphi^2 + \mathcal{O}(g^2),
$$

where $X_t = A_t - \mu/\tan \beta$. As discussed above, the heavy stop does not play any role as far as the first-order EWPT is concerned. Also, the small $m_{\tilde{t}_R}^2$ and $X_t$ are desirable. More precisely, at finite temperature, the light stop receives a thermal correction ($\Delta m_{\tilde{t}_2}^2 (T)$) which is of the order of $T^2$ to leading order. So the $m_{\tilde{t}_2}^2 + \Delta m_{\tilde{t}_2}^2 (T)$ should be vanishingly small for the strong first-order EWPT, which implies $m_{\tilde{t}_R} < 0$ since $\Delta m_{\tilde{t}_2}^2 (T) > 0$. In the LSS scenario considered in [21], the color-charge-breaking vacuum is the global minimum. On the other hand, the electroweak vacuum is metastable whose lifetime is longer than the age of the universe.

For simplicity, we take $m_{\tilde{t}_R}^2 = 0$ in the following discussion. The coefficient of cubic term in the one-loop effective potential at finite temperature is

$$
V_{\text{eff}} \geq -(E_{\text{SM}} + E_{ti}) T \varphi^3, \quad E_{ti} = \frac{y_t^4 \sin^3 \beta}{4\sqrt{2}} \left( 1 - \frac{|X_t|^2}{m_{\tilde{q}}^2} \right)^{3/2}.
$$

The deviation of $\lambda_{h hh}^{\text{MSSM}}$ from the SM value is found to be [13]

$$
\frac{\Delta \lambda_{h hh}^{\text{MSSM}}}{\lambda_{h hh}^{\text{SM}}} \simeq \frac{m_{\tilde{t}_R}^4}{2\pi^2 v^2 m_{h}^2} \left( 1 - \frac{|X_t|^2}{m_{\tilde{q}}^2} \right)^3 = \frac{2v^4}{m_{h}^2 m_{\tilde{t}_R}^2} E_{ti}^2 \simeq 0.05,
$$

where we take $m_h = 126$ GeV, $\tan \beta = 10$ and $X_t = 0$ in the last step. Unlike the 2HDM, the size of the loop effect is bounded by the top Yukawa coupling. Beyond the MSSM, however, this limit would be relaxed. For instance, in a SUSY model proposed in [22], the large enhancement is observed [23]. More examples along the same line can be found in [24].
VI. SUMMARY

In this talk, the EWBG is briefly reviewed, focusing on the nondecoupling loop properties that may induce the strong first-order EWPT as well as the large quantum corrections to the triple Higgs boson coupling. The 2HDM is the typical example that has the large nondecoupling property. Since the deviation of the triple Higgs boson coupling from the SM value is rather large, its detection at colliders [25] would be one of the experimental indications of the EWBG.

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