A spiral galaxy’s mass distribution uncovered through lensing and dynamics

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ABSTRACT

We investigate the matter distribution of a spiral galaxy with a counter-rotating stellar core, SDSS J1331+3628 (J1331), independently with gravitational lensing and stellar dynamical modelling. By fitting a gravitational potential model to a quadruplet of lensing images around J1331’s bulge, we tightly constrain the mass inside the Einstein radius \( R_{\text{Ein}} = (0.91 \pm 0.02)'' \) (\( \simeq 1.83 \pm 0.04 \) kpc) to within 4\%: \( M_{\text{Ein}} = (7.8 \pm 0.3) \times 10^{10} \text{M}_\odot \). We model observed long-slit major axis stellar kinematics in J1331’s central regions by finding Multi-Gaussian Expansion (MGE) models for the stellar and dark matter distribution that solve the axisymmetric Jeans equations. The lens and dynamical model are independently derived, but in very good agreement with each other around \( \sim R_{\text{Ein}} \). We find that J1331’s center requires a steep total mass-to-light ratio gradient. A dynamical model including an NFW halo (with virial velocity \( v_{200} \simeq 240 \pm 40 \) km \( \text{s}^{-1} \) and concentration \( c_{200} \simeq 8 \pm 2 \)) and moderate tangential velocity anisotropy (\( \beta_z \simeq -0.4 \pm 0.1 \)) can reproduce the signatures of J1331’s counter-rotating core and predict the stellar and gas rotation curve at larger radii. However, our models do not agree with the observed velocity dispersion at large radii. We speculate that the reason could be a non-trivial change in structure and kinematics due to a possible merger event in J1331’s recent past.

Key words: gravitational lensing; strong – stars: kinematics and dynamics – galaxies: kinematics and dynamics – galaxies: photometry – galaxies: structure

1 INTRODUCTION

Determining the overall mass distribution of galaxies and separating the dark matter (DM) from the stellar mass components is a crucial step in better understanding the structure and formation of galaxies and the nature of DM.

Cosmological simulations suggest that cold DM forms cuspy halos following a Navarro-Frenk-White (NFW) profile (Navarro et al. 1996). However, the existence of central DM density cusps in massive galaxies depends strongly on the stellar mass-to-light ratio (e.g., Dutton et al. 2011a), and DM dominated dwarf galaxies even favour DM halos with cores (e.g., Moore 1994; de Blok et al. 2001). This discrepancy, known as the core-cusp problem, might be resolved by galaxy formation processes such as mergers and outflows (e.g., El-Zant et al. 2001; Pontzen & Governato 2012). Especially the influence of mergers on the DM and baryonic structure of galaxies is currently an active field of research (e.g., Johansson et al. 2009; Lackner & Ostriker 2010; Hilz et al. 2012; Dutton et al. 2015).

The mass distribution of massive galaxies can be measured in completely independent fashions by gravitational lensing and dynamical modelling. Combining these two methods allows for valuable cross-checking opportunities to disentangle the galactic stellar and DM content. Massive galaxies can act as gravitational lenses, deflect the light of background sources, and give rise to multiple images. This strong gravitational lensing tightly constrains the projected total mass of the lens galaxy inside \( \sim 1'' \) (e.g., Treu 2010).

The mass profile at larger galactocentric radii can be probed by gas rotation curves that directly measure the galaxy’s circular velocity profile (e.g., Rubin et al. 1980). However, due to its dissipative nature gas motions are very sensitive to disturbances by, e.g., spiral arms and bars (e.g., Sellwood 2004). Because stars are dissipationless dynamical tracers and present almost everywhere in the galaxy, stellar dynamical modelling can complement mass constraints from lensing at small and gas motions at large radii. As stellar motions are complex—a bulk rotation around one...
principal axis combined with random motions in all coordinate directions—(Binney & Tremaine 2008), full dynamical modelling of rotation, dispersion, and velocity anisotropies is needed to deduce the matter distribution.

The Sloan WFC Edge-on Late-type Lens Survey (SWELLS, WFC = Wide field camera) (Treu et al. 2011; Dutton et al. 2011b; Brewer et al. 2012; Barnabè et al. 2012; Dutton et al. 2013; Brewer et al. 2014) is dedicated to finding and investigating spiral galaxies, which are (i) strong gravitational lenses and (ii) observed almost edge-on, such that rotation curves can be easily measured. By combining lensing and dynamical modelling, degeneracies inherent in both methods can be broken.

One of the SWELLS galaxies is the massive spiral SDSS J1331+3628, to which we refer as J1331 in the remainder of this work. It has bluish spiral arms and a large reddish bulge (see Figures 1a and 1b), which is superimposed by a quadruplet of extended bluish images approximately at a distance of 1″ from the galaxy center (see Figure 1c). The lensed object might be a star-forming blob of a background galaxy. J1331 stands out of the SWELLS sample because of its large counter-rotating core (see Figure 1d), which might be an indication that J1331 underwent a merger in its recent past.

J1331 is therefore of special interest and a convenient candidate to investigate observationally if and how a merger might have modified the DM and stellar distribution of a massive spiral galaxy. This requires in particular a precise disentanglement of stellar and DM components in the galaxy’s inner regions.

J1331 has already been the subject of several studies: Treu et al. (2011) confirmed that J1331 is a strong gravitational lens, measured its apparent brightness, and estimated the stellar masses of disk and bulge. The lensing properties of J1331 were first analysed by Brewer et al. (2012). Dutton et al. (2013) measured the gas and stellar kinematics along the major axis, and deduced J1331’s mass profile from the gas rotation curve at large radii and total mass inside the Einstein radius from gravitational lensing, focusing mostly on the outer regions of J1331.

The goal of this work is now the in-depth analysis of the matter distribution in J1331’s inner regions. This will complement the previous studies of J1331 and is an important step in understanding J1331’s merger-modified mass structure. We use stellar dynamical modelling in addition to lensing constraints, similar to a study of the Einstein Cross by van de Ven et al. (2010). We attempt to disentangle the stellar and DM components and test if employed axiymmetric Jeans models work also in the presence of a counter-rotating core.

This paper is organized as follows: Section 2 summarizes the data, Section 3 gives an overview of the modelling techniques used in this work, and Section 4 presents our results on the surface photometry of J1331 using Multi-Gaussian expansions (Section 4.1), constraints from lensing (Section 4.2) and Jeans modelling based on the surface brightness only (Section 4.3) and including an NFW DM halo (Section 4.4). Finally, Section 5 uses these results to discuss J1331’s possible merger history, stellar mass-to-light ratio, central kinematics, and starting points for future work.

2 DATA

2.1 Redshift and position

J1331 is located at right ascension = 202.9180° and declination = 36.46999° (epoch J2000). Treu et al. (2011) found from SDSS spectra that J1331 has two redshifts inside the projected radius on the sky R′ = 1″: J1331 itself has z_d = 0.113, and z_s = 0.254 is the redshift of the lensed background source (Brewer et al. 2012). According to the WMAP5 cosmology (Dunkley et al. 2009), J1331 has an angular diameter distance of 414 Mpc, which translates into a transverse scaling of 1″ ≈ 2.01 kpc. We summarize all galaxy parameters also in Table 1.

2.2 HST imaging

We use HST imaging of J1331 by Treu et al. (2011). They obtained high resolution imaging with the Hubble Space Telescope’s (HST) Wide-Field Planetary Camera 2 (WFPC2) and its WF3 CCD chip. The images are a combination of four exposures each with an exposure time of 400 sec and were drizzled to a pixel scale of 1 pixel = 0.05″. In particular, we use the images in the filters F450W, to identify the positions of the bluish lensing images, and F814W (I-band) to create a surface brightness model of the reddish bulge.

2.3 Stellar kinematics

For the dynamical modelling we use the stellar kinematics for J1331 measured by Dutton et al. (2013). They obtained long-slit spectra along J1331’s major-axis with the Low Resolution Imaging Spectrograph (LRIS) on the Keck I 10m telescope. The width of the slit was 1″ and the seeing conditions had a FWHM of ~ 1.1″. 1D spectra for spatial bins of different widths along the major axis were extracted. Line-of-sight stellar rotation velocities (vrot) and stellar velocity dispersions (σ) were determined from the spectral region containing the absorption lines Mgb (5177 Å) and FeII (5270, 5335 and 5406 Å) (analogous to Dutton et al. 2011b). Gas kinematics were extracted from Gaussian line profile fits to Hα (6563 Å) and [NI] (6583 and 6548 Å) emission lines as tracers for ionized gas.

The stellar kinematics, vrot, σ, and the root-mean-square velocity v^2 rms = v^2 rot + σ^2, are shown in Figure 1d. The rotation curve reveals a counter-rotating core within 2″ ≈ 4 kpc. Outside of ~ 3.5″ there is a drop in the dispersion. This could indicate the boundary between the pressure supported bulge and the rotationally supported disk, which appears around this radius in the F450W filter in Figure 1a. However, in the brighter F814W filter in Figure 1b the smooth reddish bulge extends out to ~ 5″.

Inside of ~ 4″ the data appears to be symmetric; outside of it the data suggests that the assumption of axisymmetry seems not to be valid anymore. We subtract 2.3 km s^-1 from vrot to ensure vrot(R' = 0) ~ 0 as a possible correction term for a misjudgement of the systemic velocity. We also symmetrize the data within 4″ and assign a minimum error of δv^2 rms = 5 km s^-1 to the v^2 rms data. In our dynamical Jeans modelling approach, which is based on the assumption of axisymmetry, only stellar kinematics with either R' ≲ 3.5″ or
Figure 1. Hubble Space Telescope (HST) images and stellar kinematics of the galaxy SDSS J1331+3628 (J1331), which has a large counter-rotating core and whose bulge acts as a strong lens for a bluish background source. Panel (a) and (b): HST/WFPC2/WFC3 images of J1331 by Treu et al. (2011) in two filters, F450W in panel (a) and F814W in panel (b). The black solid line in panel (b) shows the orientation of the major axis. Its length is 10″ and it marks approximately the region within which we carry out the dynamical modelling. Panel (c): Lensing images in the central region of J1331. An IRAF ellipse model was fitted to and then subtracted from the galaxy’s F450W surface brightness in panel (a). The (smoothed) residuals within the white square in panel (a) are shown in panel (c). The four bright blobs (A, B, C, and D), which are visible in the residuals, are arranged in a typical strong lensing configuration around the center of the galaxy (G). (The configuration of the two additional blobs which lie approximately on a line with A, B, and G does not suggest that these blobs are a lensing doublet. They might rather be star-forming regions of a background galaxy.) Panel (d): Stellar kinematics along the galaxy’s major axis as measured by Dutton et al. (2013). Shown are line-of-sight rotation velocity $v_{\text{rot}}$ (top), line-of-sight velocity dispersion $\sigma$ (middle) and the root mean-square (rms) velocity $v_{\text{rms}} = \sqrt{v_{\text{rot}}^2 + \sigma^2}$ (bottom). The dashed line indicates the galaxy’s effective half-light radius (in the F814W filter), $R_{\text{eff}} = 2.6''\pm 0.2$ kpc. The $v_{\text{rot}}$ curve reveals that J1331 has a counter-rotating core within $R_{\text{eff}}$. 
3 MODELLING

3.1 Strong gravitational lens model

3.1.1 Strong lensing formalism

A gravitational lens is a mass distribution whose gravitational potential $\Phi$ acts as a lens for light coming from a source positioned somewhere on a plane behind the lens. We summarize the basic formalism (see also Schneider et al. 1992; Narayan & Bartelmann 1996; Schneider 2006; Kochanek 2006; Treu 2010). The angular diameter distance from the observer to the lens is $D_{ls}$, to the source plane $D_s$, and the distance between the lens and source plane is $D_{ls}$. The deflection potential of the lens is its potential projected along the line of sight $z'$ and rescaled to

$$\psi(\vec{\theta}) \equiv \frac{D_{ls}}{D_{ls}D_s} \frac{2}{c^2} \int \Phi(\vec{r} = D_l \vec{\theta}, z') \, d\vec{z}'$$

(1)

where $\vec{\theta} \equiv (x', y')$ is a two-dimensional vector on the plane of the sky. The light from the source at $\vec{\beta} \equiv (x_s', y_s')$ is deflected according to the lens equation

$$\vec{\beta} = \vec{\theta}_i - \nabla_x \psi(\vec{\theta}) \bigg|_{\vec{\theta}_i}$$

(2)

into an image $\vec{\theta}_i = (x_i', y_i')$. The gradient of the deflection potential, $\nabla_x \psi(\vec{\theta})$, is equal to the angle by which the light is deflected multiplied by $D_{ls}/D_s$.

The inverse magnification tensor

$$\mathcal{M}^{-1} \equiv \frac{\partial^2 \vec{\beta}}{\partial \vec{\theta}^2} \bigg|_{\vec{\theta}_i} \equiv \left( \begin{array}{cc} \delta_{ij} - \frac{\partial^2 \psi}{\partial \theta_i \partial \theta_j} & 0 \\ 0 & \frac{\partial^2 \psi}{\partial \theta_i \partial \theta_j} \end{array} \right)$$

(3)

describes how the source position changes with image position, the distortion of the image shape for an extended source and its magnification $\mu \equiv$ image area/source area $= \det \mathcal{M}$. Lines in the image plane for which the magnification becomes infinite, i.e., $\det \mathcal{M}^{-1} = 0$, are called caustics. The corresponding lines in the source plane are called caustics. The position of the source with respect to the caustic determines the number of images and their configuration and shape with respect to each other.

The Einstein mass $M_{\text{Ein}}$ and Einstein radius $R_{\text{Ein}}$ are defined via the relation

$$M_{\text{Ein}} \equiv M(< R_{\text{Ein}}) \equiv \pi \Sigma_{\text{crit}} R_{\text{Ein}}^2$$

(4)

where

$$\Sigma_{\text{crit}} \equiv \frac{c^2}{4\pi G D_{ls}D_sD_{ls}}$$

(5)

is the critical density and $M(< R_{\text{Ein}})$ is the mass projected along the line-of-sight within $R' = R_{\text{Ein}}$. $M_{\text{Ein}}$ is similar to the projected mass within the critical curve $M_{\text{crit}}$.

3.1.2 Lens model

Following Evans & Witt (2003) we assume a scale-free model

$$\psi(R', \theta') = R'^\alpha F(\theta')$$

(6)

for the lensing potential, consisting of an angular part $F(\theta')$ and a radial power-law part, with $(R', \theta')$ being again polar coordinates on the plane of the sky. $\alpha$ denotes the rotation curve slope of the lens and the case $\alpha = 1$ corresponds to a flat rotation curve. The surface density of this model is

$$\Sigma(R', \theta') = \frac{\Sigma_{\text{crit}}}{2} \left( \alpha^2 F(\theta') + \frac{\partial^2 F(\theta')}{\partial \theta'^2} \right) R'^{\alpha-2}.$$ 

We expand $F(\theta')$ into a Fourier series,

$$F(\theta') = \frac{a_0}{2} + \sum_{k=1} a_k \cos(2k\theta') + b_k \sin(2k\theta').$$

(7)

For this scale-free lens model the lens equation (2) becomes

$$\begin{pmatrix} x_i' \\ y_i' \end{pmatrix} = \begin{pmatrix} R_c' \cos \theta_i' - R_c'^{-1} (\alpha \cos \theta_i' F(\theta_i') - \sin \theta_i' F'(\theta_i')) \\ R_c' \sin \theta_i' - R_c'^{-1} (\alpha \sin \theta_i' F(\theta_i') + \cos \theta_i' F'(\theta_i')) \end{pmatrix}$$

(8)

(Evans & Witt 2003), where $F'(\theta') \equiv \partial F(\theta')/\partial \theta'$. When we fix the slope $\alpha$, then the lens equation is a purely linear problem and can be solved numerically for the source position $(x_i', y_i')$ and the Fourier parameters $(a_k, b_k)$ given one observed image at position $(x_i', y_i')$.

3.1.3 Model fitting

The free parameters of the lens model are: the source position $(x_s', y_s')$, the radial slope $\alpha$ and Fourier parameters $(a_k, b_k)$ of the lens mass distribution in Equations (6)-(7). We want to minimize the distance between the observed image positions, $\theta_{\text{obs}}$, and those predicted by the lensing model, $\theta_{\text{pre}}$. To avoid having to solve the lens equation (8) for $\theta_{\text{pre}}$, we follow Kochanek (1991) and cast the calculation back to the source plane using the magnification tensor in Equation (3) to approximate $\theta' \simeq (\partial \theta' / \partial \beta) \delta = \mathcal{M} \delta$. The best-fitting lens model is then the one that minimizes

$$\chi^2_{\text{lens}} = \sum_i \left( \left| \begin{array}{c} \frac{x_i'}{D_{ls}} \\ 0 \\ \frac{0}{D_{ls}} \end{array} \right| \bar{\theta}_{\text{pre}} - \bar{\theta}_{\text{obs}} \right|^2,$$

(9)

where $(\Delta_x, \Delta_y)$ are the measurement errors of the image positions $\theta_{\text{obs}}$. $\mathcal{M}|_{\bar{\theta} = \bar{\theta}_{\text{obs}}}$ is the magnification tensor and $(\bar{x}_{\text{pre}}, \bar{y}_{\text{pre}})$ the source position according to the lens equation, both evaluated at the position of the $i$-th lensing image, $\theta_{\text{obs}}$. Following van de Ven et al. (2010) we add a term

$$\chi^2_{\text{shape}} = \lambda \sum_{k \geq 3} \left( \frac{a_k^2 + b_k^2}{a_0^2} \right)$$

(10)

(with $\lambda$ being some weight factor) which forces the shape of the mass distribution to be close to an ellipse. The total $\chi^2$ to minimize is therefore

$$\chi^2 = \chi^2_{\text{lens}} + \chi^2_{\text{shape}}$$

(11)
We set $a_1 = b_1 = 0$, which corresponds to the choice of origin; in this case the center of the galaxy.

To be able to constrain the slope $\alpha$ we would need flux ratios for the images as in van de Ven et al. (2010). But the extent of the images, possible dust obscuration and surface brightness fluctuations due to microlensing events, as well as the uncertainty in surface brightness subtraction, make flux determination too unreliable and we do not include them in the fitting.

### 3.2 Surface brightness model

#### 3.2.1 Multi-Gaussian Expansion (MGE)

MGEs are used to parametrize the observed surface brightness (or projected total mass) of a galaxy as a sum of $N$ two-dimensional, elliptical Gaussians (Bendinelli 1991; Monnet et al. 1992; Emsellem et al. 1994, 1999). This work makes use of the algorithm and code\(^1\) by Cappellari (2002).

We assume all Gaussians to have the same center and position angle $\phi$, i.e., the orientation of the Gaussians’ major axis measured from North through East in the polar coordinate system $(R', \theta')$ on the plane of the sky. Then a surface brightness model can be expressed as

$$I(R', \theta') = \sum_{i=1}^{N} I_{0,i} \exp \left[ -\frac{1}{2\sigma_i^2} (x^2_i + y^2_i) \right]$$

with $I_{0,i} = \frac{L_i}{2\pi \sigma_i}$ and $x_i = R \cos(\theta' - \phi)$, $y_i = R \sin(\theta' - \phi)$, $\sigma_i$ its dispersion along the major axis and $\beta_i$ the axis ratio between the elliptical Gaussian’s major and minor axis.

#### 3.2.2 Convolution with the point spread function (PSF)

We can also expand the telescope’s PSF as a sum of circular Gaussians,

$$\text{PSF}(x', y') = \sum_j G_j \exp \left[ -\frac{1}{2\delta_j^2} (x^2 + y'^2) \right].$$

The observed surface brightness distribution is a convolution of the intrinsic surface brightness in Equation (12) with the PSF in Equation (15): $(I \ast \text{PSF})(x', y')$ is then again a sum of Gaussians and can be directly fitted to an image of the galaxy in question.

\[^1\] The IDL code package for fitting MGEs to images by Cappellari (2002) is available online at [http://www-astro.physics.ox.ac.uk/~mxc/software](http://www-astro.physics.ox.ac.uk/~mxc/software). The version from June 2012 was used in this work.

### 3.3 Axisymmetric dynamical model

#### 3.3.1 Jeans Anisotropic Models (JAM)

JAM modelling assumes galaxies to be (i) collisionless, (ii) in a steady state, and (iii) axisymmetric. With these assumptions the axisymmetric Jeans equations follow from the vector-valued first moment of the collisionless Boltzmann equation (see Equations (4.221)-(4.222) in Binney & Tremaine (2008)). The Jeans equations are functions of the second velocity moments $(\langle v_i v_j \rangle)$ with $i, j \in (R, z, \phi)$, the number density of (stellar) tracers $n(\vec{x})$, and the galaxy’s gravitational potential $\Phi(\vec{x})$ generated by the mass density $\rho(\vec{x})$.

To be able to solve the Jeans equations, additional assumptions about the velocity ellipsoid tensor $(\langle v_i v_j \rangle)$ have to be made. We follow Cappellari (2008) and assume first that the galaxy’s velocity ellipsoid is aligned with the cylindrical coordinate system, i.e., $(\langle v_R v_z \rangle = \langle v_v v_{v_R} \rangle = \langle v_v v_{v_B} \rangle = 0$. Secondly, we assume a constant ratio between the radial and vertical second velocity moments,

$$\beta_z \equiv \frac{\langle v_z^2 \rangle}{\langle v_R^2 \rangle},$$

where $\beta_z$ is the velocity anisotropy parameter.

The JAM modelling approach by Cappellari (2008) expresses the tracer and mass density in terms of MGEs (see also Emsellem et al. 1994). The tracer density $n(\vec{x})$ is assumed to be proportional to the observed and deprojected brightness distribution $\nu(R, z)$ in Equation (16). The mass density $\rho(R, z)$ can consist of several sets of MGEs, describing stellar and DM components. The MGE for $\Phi(R, z)$ is generated from the mass density MGE by integrating the Poisson equation (Emsellem et al. 1994).

\[^2\] $(R, z)$ are cylindrical coordinates aligned with the galactic plane. The primed $(R', z')$ denote polar coordinates on the plane of the sky.
In this way one can now calculate an unambiguous model prediction for the velocity dispersion tensor \( \langle v_i v_j \rangle(R, z) = \langle \sigma_i^2 \rangle(R, z) \) (with \( i, j \in \{ R, \phi, z \} \) and \( v_i v_j = 0 \) if \( i \neq j \)). To compare it with observations, \( \langle v_i^2 \rangle(R, z) \) has to be rotated by the inclination angle \( i \) to the coordinate system of the observer; \( x', y' \) is the plane of the sky and \( z' \) the line-of-sight, where \( x' \) is aligned with the galaxy’s major axis. Taking a light-weighted projection along the line-of-sight gives a model prediction for the line-of-sight velocity second moment \( \langle v_{\text{los}}^2 \rangle(x', y') \), which is comparable to actual spectroscopic measurements of the second velocity moment. Details of the derivation of \( \langle v_{\text{los}}^2 \rangle(x', y') \) from the Jeans equations using the MGE formalism are laid out in Cappellari (2008) and in the appendix of van de Ven et al. (2010). The result for \( \langle v_{\text{los}}^2 \rangle(x', y') \) in particular is given in Equation (28) and Equation (A18), respectively.

The JAM modelling code\(^3\) by Cappellari (2008) evaluates this expression for \( \langle v_{\text{los}}^2 \rangle(x', y') \) numerically for a given luminous tracer and mass distribution MGE and a given inclination.

### 3.3.2 Data comparison

As data we use stellar line-of-sight rotation velocities \( v_{\text{rot}} = \langle v_{\text{los}} \rangle_{\text{obs}} \) and velocity dispersions \( \sigma \) as described in Section 2.3. The JAM models give a prediction for the second line-of-sight velocity moment \( \langle v_{\text{los}}^2 \rangle_{\text{obs}} \). The root-mean-square (rms) line-of-sight velocity \( v_{\text{rms}} \) allows a data-model comparison by relating theses velocities according to

\[
\sigma^2 = v_{\text{rms}}^2 = v_{\text{rot}}^2 + \sigma^2 \equiv \langle v_{\text{los}}^2 \rangle_{\text{obs}}.
\]

The model derived from the Jeans equations as outlined in Section 3.3.1 predicts the intrinsic \( \langle v_{\text{los}}^2 \rangle_{\text{obs}} \equiv \langle v_{\text{los}}^2 \rangle \) at a given position on the sky, which needs then to be modified to \( \langle v_{\text{los}}^2 \rangle_{\text{obs}} \) according to the mode of observation to be comparable to the measurements. The measured \( v_{\text{rms}} \) in this work is a light-weighted mean for a pixel along the long-slit of the spectrograph, with width \( L_y = 1'' \) (Dutton et al. 2013) and a certain given extent along the galaxy’s major axis, \( L_z \), i.e., for a rectangular aperture

\[
\text{AP}(x', y') \equiv \begin{cases} 
1 & \text{for } -\frac{L_z}{2} \leq x' < +\frac{L_z}{2} \\
0 & \text{otherwise}
\end{cases}
\]

and \( -\frac{L_y}{2} \leq y' \leq +\frac{L_y}{2} \).

The root-mean-square of the observed light 

\[
\text{PSF}(x', y') \equiv \mathcal{N}(0, \sigma_{\text{seeing}} = \text{FWHM}/2\sqrt{2\ln 2}).
\]

The model predictions for \( \langle v_{\text{los}}^2 \rangle_{\text{obs}} \) have therefore to be convolved with the convolution kernel

\[
K(x', y') = 1 + \prod_{u \in \{x', y'\}} \text{erf} \left( \frac{L_y/2 - u}{\sqrt{2} \sigma_{\text{seeing}}} \right)
\]

and weighted by the surface brightness \( I(x', y') \), i.e.,

\[
\langle v_{\text{los}}^2 \rangle_{\text{obs}} = I * K,
\]

\[
\langle v_{\text{los}}^2 \rangle_{\text{obs}} = (I \langle v_{\text{los}}^2 \rangle_{\text{obs}}) * K.
\]

We modified the JAM code by Cappellari (2008) to use this convolution kernel with non-square pixels. The JAM code then performs the convolution numerically. We set \( L_x = 0.21'' \) as the width of the model pixel, and get a prediction for the actual measurements in bins of width 0.63\(^{\prime}\), 1.26\(^{\prime}\) and 1.89\(^{\prime}\) (Dutton et al. 2013) as light-weighted mean from each 3, 6 and 9 model pixels.

### 3.3.3 Rotation curve

The intrinsic galaxy rotation curve is the first velocity moment \( \langle v_{\phi} \rangle = \sqrt{\langle v_{\phi}^2 \rangle - \sigma^2} \). The observed rotation velocity is the projection of the light-weighted contributions to \( \langle v_{\phi} \rangle \) along the line-of-sight (Equation (31) in Cappellari (2008)).

The first velocity moments cannot be uniquely determined from the Jeans equations, which give only a prediction for the second velocity moments. Further assumptions are needed to separate the second velocity moments into ordered and random motion. Cappellari (2008) assumes that in a steady state there is no streaming velocity in \( R \), i.e., \( \langle v_R \rangle = 0 \), and therefore \( \sigma^2_R = \langle v_{\phi}^2 \rangle \). Then Cappellari (2008) relates the dispersions in \( R \) and \( \phi \) direction such that

\[
\langle v_{\phi} \rangle = \sqrt{\langle v_{\phi}^2 \rangle - \sigma^2_R} \equiv \kappa \langle v_{\phi}^2 \rangle / \langle v_{\phi}^2 \rangle
\]

and the \( \kappa \) parameter quantifies the rotation: \( \kappa = 0 \) means no rotation at all, and \( |\kappa| = 1 \) describes a velocity dispersion ellipsoid that is a circle in the \( R-\phi \) plane (Cappellari 2008). The sign of \( \kappa \) determines the rotation direction. We can assign a constant \( \kappa \) to every Gaussian in the MGE formalism and calculate the light-weighted circular velocity curve, given the second velocity moments found from the Jeans equations (see Equations (37) and (38) in Cappellari (2008)) for the intrinsic and observed rotation curves, respectively.

To model the counter-rotating core of J1331 with one free parameter, we employ the condition that the overall \( \kappa(R) \) profile should smoothly and relatively steeply transit from \( \kappa(R) = -\kappa' < 0 \) at small \( R \) through \( \kappa(R_0) = 0 \) and increase to \( \kappa(R) = \kappa' > 0 \) at large \( R \). Our imposed profile is

\[
\kappa(R) \equiv \kappa' R_0^2 / [R^2 + R_0^2].
\]

We find \( \kappa' \) by matching the model \( \langle v_{\text{los}} \rangle_{\text{obs}} \) with the symmetrized \( v_{\text{rot}} \) data, where for a given \( \kappa' \) the \( \kappa_i \) are found from fitting the MGE generated profile \( \kappa(R) = \sum \kappa_i v_i(r) / \sum v_i(r) \) to Equation (27). The observed zero-point is at \( R_0 \approx 2'' \). In the deprojected galactic plane the
Table 1. General galaxy parameters of J1331.

| Parameter                          | Value (Brewer et al. 2012) |
|-----------------------------------|----------------------------|
| redshift                          | $z_d$                      | 0.113 |
| angular diameter distance         | $D_A$ (Mpc)                | 414   |
| scaling                           | $1$ kpc/$M^2$              | 2.006 |
| position angle from North         | $\phi$ [°]                 | 42.90 |
| average axis ratio                | $q'$                       | 0.598 |
| average ellipticity              | $e = 1 - q'$               | 0.402 |
| estimated inclination            | $\iota$ [°]                | 70    |
| apparent I-band magnitude        | $I_{1331}$ [mag]           | 15.77 |
| total I-band luminosity           | $L_{\text{I},\text{tot}}$ [10^{10}L_\odot] | 5.6 |
| effective half-light radius       | $R_{\text{eff}}$ ["]      | 2.6   |
|                                  | $R_{\text{eff}}$ [pc]      | 5.2   |

radius of zero rotation would be at $R_0 \gtrsim 2''$, and we choose it to be at $2.2''$.

3.3.4 Including an NFW halo

As mentioned above, JAM modelling allows us to incorporate an invisible matter component in addition to the luminous matter in the form of an MGE. In Section 4.4, we will include a spherical Navarro-Frenk-White (NFW) DM halo (Navarro et al. 1996) in the dynamical model. The classical NFW profile has the form

$$\rho_{\text{NFW}}(r) \propto r^{-1} (r + r_s)^{-2} \quad (28)$$

and two free parameters, the scale length $r_s$ and a parameter describing the total mass of the halo. We will use $v_{200} \equiv \sqrt{GM_{200}/r_{200}}$, which is the circular velocity at the radius $r_{200}$ within which the mean density of the halo is 200 times the cosmological critical density $\rho_{\text{crit}} \equiv (2H^2)/(8\pi G)$, and where $M_{200} \equiv M(<r_{200}) \equiv 4\pi r_{200}^3 \times 200\rho_{\text{crit}}(z = 0)$, with $\rho_{\text{crit}}(z = 0) = 1.43 \times 10^{-3}M_\odot/\text{pc}^3$ in the WMAP5 cosmology by Dunkley et al. (2009). The mass concentration of the NFW halo is quantified by $c_{200} \equiv r_{200}/r_s$. There is a close relation between the concentration and halo mass in simulations (Navarro et al. 1996). Macciò et al. (2008) found this relation for the WMAP5 cosmology to be

$$(\log c_{200})(M_{200}) = 0.830 - 0.098 \log \left( \frac{M_{200}}{10^{12}M_\odot} \right) \quad (29)$$

(their Equation 10), with a Gaussian scatter of $\sigma_{\log c_{200}} = 0.105$ (their Table A2). In Section 4.4, we will use this relation as prior information to guide the modelling towards realistic NFW halo shapes.

4 RESULTS

4.1 Surface photometry for J1331 with MGEs

In this section we construct a model for J1331’s intrinsic light distribution in terms of MGEs (see Section 3.2). We use the HST image in the F814W (I-band) filter (Figure 1b) because J1331’s central stellar component appears at longer wavelengths (ii) smoother and more extended than in the F450W filter (Figure 1a), as it is less sensitive to young clumpy star-forming regions, (ii) much brighter than the bluish lensing images, and (iii) the imaging is less prone to extinction.

| $j$ | $G_j$ | $\delta_j$ ["] |
|-----|-------|----------------|
| 1   | 0.184 | 0.038 |
| 2   | 0.485 | 0.085 |
| 3   | 0.222 | 0.169 |
| 4   | 0.109 | 0.487 |

4.1.1 PSF for the HST/F814W filter

The one-dimensional MGE in Equation (15) is fitted to the radial profile of a synthetic image of the HST/F814W filter PSF, ignoring diffraction spikes and using the code by Cappellari (2002). The MGE parameters of the normalized PSF model are given in Table 2.

4.1.2 MGE for the inner and outer regions

We fit a MGE to J1331’s smooth central region within $\sim 5''$ of the HST/WFPC2/WF3/F814W image (Figure 1b). Bright objects close to the bulge (blobs possibly belonging to the background galaxy and parts of the foreground spiral arm) were masked during the fit. J1331’s galaxy center, position angle (with respect to North through East), and average apparent ellipticity (see Table 1) are found from the images weighted first and second moment. The MGE fit splits the image in annuli with the given ellipticity and position angle and sectors of 5'' width and fits an 5-Gaussian MGE of the form in Equation (12) convolved with the PSF MGE in Table 2 to it. The best-fitting MGE (PSF convolved) is compared to the data in Figure 2a, and the corresponding parameters of the intrinsic surface brightness distribution are given in Table 3. The fit is a very good representation of the light distribution in the inner 5'', but underestimates the light distribution further out.

To get a handle on the light distribution also in the outer parts of J1331 where spiral arms dominate, we fit an IRAF (Tody 1993) ellipse model to the F814W image (masking the brightest blobs in the spiral arms and outer regions). Only then we fit a 7-Gaussian MGE to the smooth ellipse model. The MGE does not perfectly reproduce the flatness of the ellipse model at every radius (see Figure 2b), but considering the spiral arm dominated outer regions of J1331 it is good enough for an approximate handling of the overall light distribution.

4.1.3 Transformation into physical units

To transform the MGE in units of counts into physical units, we apply a simplified version of the procedure described in Holtzman et al. (1995).

The scaling of the drizzled HST/WFC3 images is $S \equiv 0.05''$/pixel width and the total exposure time $T = 1600$ sec. Each Gaussian in the MGE has a total F814W luminosity $L_i$ (in counts) and a central surface brightness (in counts per pixel) of

$$C_{0,i} \text{[counts/pixel]} = \frac{L_i \text{[counts]}}{2\pi \sigma_i \text{[pixel]}^2 q_i}. \quad (30)$$

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Figure 2. MGEs for J1331’s surface brightness distribution. Comparison of contours with constant F814W surface brightness (orange lines) with the corresponding iso-brightness contours of the best-fitting MGE, convolved with the PSF in Table 3, (grey lines). The black line has a length of 10″ and its orientation corresponds to the galaxy’s position angle as found in Table 1. For comparison, the Einstein radius as found in Table 5 is indicated as red dashed circle. Panel (a): Central regions of J1331. The MGE model is a good representation of the galaxy’s light distribution along the major axis within ∼ 5″. Its parameters are given in Table 3. This MGE is used as model for the stellar tracer distribution in the dynamical Jeans modelling in Sections 4.3 and 4.4. Panel (b): Outer regions of J1331. The orange lines indicate here contours of a smooth IRAF ellipse fit to J1331 in the F814W filter; the grey lines are the corresponding best-fitting MGE. This MGE is not used for dynamical model fitting because the dynamics in the outer regions are strongly affected by non-axisymmetries (e.g., spiral arms). We use it, however, to estimate the galaxy’s total luminosity and effective radius, and to get an estimate for the dynamics of the outer regions.

Table 3. Parameters of the best-fitting MGE to the F814W surface brightness of J1331 in Figure 2a. The fit is best inside a radius of 5″. The position angle is given in Table 1. This MGE is used in the dynamical modelling in Sections 4.3 and 4.4. The first column gives for each Gaussian the total F814W luminosity in Equation (13) in units of counts. The second column is the corresponding I-band peak surface brightness in Equation (12) in units of a luminosity surface density. The third and fourth column give the dispersion and the last column the axis ratio of the Gaussian in Equation (12).

| i  | $L_i$ [counts] | $I_{0,i} [L_\odot/pc^2]$ | $\sigma_i ["]$ | $\sigma_i [kpc]$ | $q_i'$ |
|----|----------------|--------------------------|----------------|-----------------|-------|
| 1  | 9425.96        | 20768.0                  | 0.051          | 0.103           | 1.00  |
| 2  | 13173.0        | 3161.2                   | 0.178          | 0.358           | 0.76  |
| 3  | 40235.0        | 1588.2                   | 0.503          | 1.008           | 0.58  |
| 4  | 67755.2        | 502.25                   | 1.180          | 2.368           | 0.56  |
| 5  | 203677.0       | 136.51                   | 3.891          | 7.805           | 0.57  |

This is then transformed into an I-band surface brightness (in mag × (1")⁻²) via

$$\mu_{I,0,i} = -2.5 \log_{10} \left( \frac{C_0 [\text{counts/pixel}]}{[\text{sec}] \times 5\"/\text{pixel width}} \right)^2 + Z + C + A_I,$$

(31)

where $Z \simeq 21.62$ mag is the zero-point from Holtzman et al. (1995), updated according to Dolphin (2000)⁴, for the photometric system of the HST/WFPC2 camera and the F814W filter, plus a correction for the difference in gain between calibration and observation. $C = 0.1$ mag corrects for the finite aperture of the WFPC2; and $A_I = 0.015$ mag is the extinction in the (Landolt) I-band towards J1331, according to the NASA/IPAC Extragalactic Database (NED)⁵. The colour-dependent correction between the F814W filter and the I-band of the UBVRI photometric system is small (Holtzman et al. 1995) and we neglect it therefore. The last step is to transform the surface brightness $\mu_{I,0,i}$ (in mag) to the I-band surface density $I_{0,i}$ (in $L_\odot/pc^2$) of the Gaussian.

⁴ We used the updated zero points by Andrew E. Dolphin, "Zero Points relative to Holtzman et al. (1995)" from http://americano.dolphinsim.com/wfpc2_calib/2008_07_19.html. The data was retrieved on September 20th, 2013.

⁵ The NASA/IPAC Extragalactic Database (NED, https://ned.ipac.caltech.edu/) is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration. The data for J1331 (SDSS J133140.33+362811.9) was retrieved in October 2013.
The luminosity $L_\text{I} = 0.4$ mag is the Sun’s absolute $I$-band magnitude (Binney & Merrifield 1998). The luminosity $L_\odot [\text{counts}]$ and the corresponding surface brightness density $I_\odot [L_\odot \text{pc}^{-2}]$ of each Gaussian are given in Table 3.

4.1.4 Inclination, total luminosity, and effective radius

To estimate the inclination of J1331 with respect to the observer, we use the observed axis ratio of the flattest ellipse in the IRAF ellipse model for J1331, which is $q' = 0.42$. This is similar to the disk axis ratio of $q = 0.40$ found by Treu et al. (2011). If a typical thickness of an oblate disk is around $q_0 \sim 0.2$ (Holmberg 1958), the inclination follows from

$$\cos^2 \theta = \frac{q'^2 - q_0^2}{1 - q_0^2}$$

and a correction of $+3^\circ$ (Tully 1988). Our estimate for the inclination is therefore $\theta \approx 70^\circ$. Given this inclination, the two-dimensional MGE models can be deprojected into three dimensions (see Section 3.2.3). We also assume the inclination angle to be known and fixed to this value in the dynamical modelling in Sections 4.3 and 4.4.

J1331’s total $I$-band luminosity is determined by summing up the luminosity contributions of all the MGE Gaussians for the outer regions (shown as grey lines in Figure 2b). We find $L_{I,\text{tot}} \approx 5.6 \times 10^{10} L_\odot$. This corresponds to an apparent magnitude of $m_I = 15.77$ mag. We determine the circularized effective radius $R_{\text{eff}}$ of J1331 from the definition $L(< R_{\text{eff}}) \equiv \frac{1}{2} L_{I,\text{tot}}$ and the growth curve $L(< R')$ from the MGE model of the outer regions, where $R'$ is the projected radius on the sky. We find the effective radius to be $R_{\text{eff}} \approx 2.6'' \approx 5.2$ kpc.

All galaxy parameters are summarized in Table 1.

4.2 Mass distribution from lensing

In this section we use the gravitational lensing formalism summarized in Section 3.1 to fit a scale-free galaxy mass model to the positions of the lensing images observed in J1331’s central region.

4.2.1 Image positions

We determine the positions of the lensing images by first subtracting a smooth model for the galaxy’s surface brightness from the original image. As models we use MGE fits and IRAF ellipse fits to J1331 in each the F450W and F814W filter. The lensing images become visible in the residuals (see Figure 1c). Because the images are extended, we use the position of the brightest pixel in each of the images. In addition, we consider the F450W-MGE subtracted residuals from Brewer et al. (2012). The lensing positions, as determined from the latter, are given in Table 4. The scatter of lensing positions, as determined from subtracting different brightness models from the galaxy in different filters, gives an error of $\pm 1$ pixel on the image positions. To the galaxy center, which we assume to be the surface brightness peak in the F450W image, we apply an error of $\pm \sqrt{2}$ pixel.

Eight image position coordinates allow us to fit a lens mass model with only $< 8$ free parameters. We therefore do not fit Fourier components $(a_k, b_k)$ with $k > 3$ in the lens mass model in Equations (6)-(7).

Even though the constraint from the image positions on $\alpha$ is very weak, we were able to show that the image positions in Table 4 are consistent with a model with flat rotation curve. In the following we therefore set $\alpha = 1$. 

---

**Table 4.** Positions of the lensing images (A-D) and the galaxy center (G) in Figure 1c. The image positions were determined from the lens-MGE subtracted F450W image for J1331 by Brewer et al. (2012) (their Figure 4), rotated to the ($x', y'$) coordinate system in Figure 1c. The pixel scale is 1 pixel = 0.05″ and the error of the image positions A-D is $\pm$ 1 pixel.

|   | A   | B   | C   | D   | G   |
|---|-----|-----|-----|-----|-----|
| $x'_{\text{[pixel]}}$ | 12.1 | -8.5 | 21.7 | -3.3 | 0.5 ± $\sqrt{2}$ |
| $y'_{\text{[pixel]}}$  | 16.6 | -10.4 | -0.5 | 19.2 | 0.5 ± $\sqrt{2}$ |

---

**Figure 3.** Lensing model (in Table 5) found as best fit to the lensing image positions. In the background we show the central region of J1331 in the F450W filter, subtracted by an IRAF ellipse model of the F450W surface brightness and smoothed to remove noise smaller than the PSF. The brightness peaks of the four lensing images and the galaxy center (Table 4) are marked as red dots. For the best-fitting lens model we show the Einstein radius (red dotted circle) and the critical curve (red solid line), which are located in the lens plane. We also show the caustic (green solid line) corresponding to the critical curve and the best-fitting source position (green dot), which are located in the source plane. For $\alpha = 1$, the critical curve is a contour of constant surface density of the mass model. The grey lines show contours of the time delay surface given by Equation (63) in Narayan & Bartelmann (1996). Not only the position of the extremum, but also their shape is consistent with the observed, extended images, even though we did not use information about the image shape in the analysis.
The smooth black contours correspond to the best-fitting model’s time delay surface (see Figure 3). The corresponding critical curve is also an equidensity contour of the galaxy (see Equations (9)-(11)). The best-fitting parameters are given in the first column of Table 5. Figure 3 shows the corresponding critical curve, caustic and Einstein radius, and the best-fitting source position. In this case, where \( \alpha = 1 \), the (tangential) critical curve is also an equidensity contour of the galaxy model (Evans & Witt 2003), which appears to have an elliptical mass distribution. The source is located close to a cusp of the diamond-shaped caustic: a lensing configuration for which we indeed expect four images. Figure 3 also shows the (smoothed) residuals from the F450W image subtracted by an IRAF ellipse brightness model and the contours of the best-fitting model’s time delay surface (see §3.3.1 in Narayan & Bartelmann 1996). Fermat’s principle states that the image positions are observed at the extrema of the time delay surface. And even though we did not include any information about the shape of the lensing images in the fit, it is consistent with the predicted distortion for an extended source.

To estimate how the uncertainties in the determination of image positions and galaxy center affect the results, we sample random positions from two-dimensional Normal distributions with peaks and standard deviations according to Table 4. Model fits to many sampled image positions lead to probability distributions for the best-fitting shape parameters and Einstein quantities; peak and standard deviations are given in the second column of Table 5. We constrain the Einstein radius to within 2\%,

\[
R_{\text{ein}} = (0.91 \pm 0.02)\text{\,kpc, and the projected mass within the critical curve with a relative error of 4\%,} \quad M_{\text{crit}} = (7.9 \pm 0.3) \times 10^{10}\text{\,M}_\odot. \quad \text{Our measurement of} \ R_{\text{ein,SWELLS}} = (0.96 \pm 0.04)\text{\,kpc (which used a singular isothermal ellipsoid as lens mass model and the intermediate-axis convention of the critical curve as the Einstein radius). The relative difference between our critical mass and that of Brewer et al. (2012),} \ \ M_{\text{crit,SWELLS}} = (8.86 \pm 0.61) \times 10^{10}\text{\,M}_\odot, \text{is 13\%.}
\]
4.2.3 Comparison with the light distribution

The surface mass distribution as predicted by the best-fitting lens model (Table 5) is shown in Figure 4b. We visualize the effect of the Fourier shape parameter uncertainties by introducing random noise to create a mock observation. From the mock image’s second moment we find an average axis ratio for the lens mass model of \(q_{\text{lens}} \approx 0.695\), which is consistent with the one found by Brewer et al. (2012), \(q_{\text{lens, SWELLSHI}} = 0.67 \pm 0.09\), while the light’s average axis ratio is \(q' = 0.598\) (see Table 1).

We estimate the total (projected) mass-to-light ratio within the Einstein radius \(\Upsilon_{\text{Ein}}^{\text{tot}} = M_{\text{Ein}}/L_{\text{Ein}}\). For this, we integrate the MGE in Table 3 to get the total I-band luminosity within the Einstein radius \(L_{\text{Ein}} = 1.40 \times 10^{10} L_{\odot}\). The corresponding Einstein mass-to-light ratio is therefore \(\Upsilon_{\text{Ein}}^{\text{tot}} = 5.56 \Upsilon_{\odot}\). This is consistent with or slightly larger than the stellar mass-to-light ratio assuming a Salpeter initial mass function (IMF) \(\Upsilon_{\odot} = 4.7 \pm 1.2\) according to Treu et al. (2011) and Table 7 (see also discussion in Section 5.2).

We use \(\Upsilon_{\text{Ein}}^{\text{tot}}\) to transform the observed surface brightness in the F814W filter into a surface mass density (Figure 4a). Figure 4c then compares equidensity contours of both the predicted lens mass distribution and the observed surface brightness times \(\Upsilon_{\text{Ein}}^{\text{tot}}\).

Figure 4 leads to the following three findings: (i) The mass predicted from lensing and the observed light distribution are oriented in the same direction (i.e., have the same position angle). (ii) Within and around the Einstein radius, mass and light distribution have a similar elliptical shape, while further out the mass distribution is slightly rounder. (iii) The light distribution drops faster than the mass with increasing radius (which is—at least partly—because of the assumption of a flat rotation curve). However, the mass distribution is only constrained around the Einstein radius and otherwise is an extrapolation.

4.3 JAM based on surface brightness

In this section we create dynamical models for J1331 following the procedure in Sections 3.3.1–3.3.2. We use the deprojected surface brightness MGE from Table 3 for the tracer distribution \(\nu(R, z)\) and to generate mass models \(\rho(R, z)\) (assuming the galaxy’s inclination angle to be \(\iota = 70^\circ\); see Table 1 and Section 4.1.4). The only exception is the first test, where the mass model comes from lensing constraints.

4.3.1 JAM with lens mass model

We make an independent prediction for the \(v_{\text{rms}}\) curve by evaluating the JAM equations (with \(\beta_x = 0\)) for the lens mass model in Table 5 (\(\alpha = 1\), flat rotation curve). In addition, we also calculate a \(v_{\text{rms}}\) curve for two lens models which were found analogously, but assumed a slightly rising (falling) rotation curve slope of \(\alpha = 1.1\) (\(\alpha = 0.9\)). The predictions are compared with the data in Figure 5. While the most reliable constraint is around \(R_{\text{Ein}}\), the agreement within \(R' \sim 3''\) is still striking: The \(\alpha > 1\) model recreates the observed central dip, while the \(\alpha = 1\) model fits the wings around \(R_{\text{eff}}\). This is in concordance with observations in other galaxies. For \(R' > R_{\text{eff}}\) we would expect \(\alpha < 1\); and the lensing model for \(\alpha = 0.9\) has indeed a slightly dropping \(v_{\text{rms}}\) around \(R_{\text{eff}}\) like the data. A definite comparison in this regime is however difficult as the lens models are just extrapolations outside of \(R_{\text{Ein}}\). While our lensing model assumes \(\alpha(R') = \text{const}\), Figure 5 suggests that a model with variable...
Figure 7. (a) Comparison of $v_{\text{rms}}$ data and best-fitting model. (b) Projected local mass-to-light ratio profile and enclosed mass.

$\alpha(R')$ could fit even better. Overall the lensing model is in very good agreement with the $v_{\text{rms}}$ data within $R' \sim 3''$, even though it was derived completely independently.

4.3.2 JAM with "mass-follows-light" and velocity anisotropy

The first JAM model that we fit to the observed $v_{\text{rms}}$ within $R' < 5''$ is a mass-follows-light model. Mass-follows-light models are often used in dynamical JAM modelling (e.g., van de Ven et al. 2010; Cappellari et al. 2006) and generate a mass distribution by multiplying the intrinsic light distribution $\nu(R,z)$ by a constant total mass-to-light ratio $\Upsilon_{1,\text{tot}}$. This assumes that the DM is always a constant fraction of the total matter distribution within the region covered by the kinematics. This simplified mass model sometimes gives good representations of the inner parts of galaxies where the stellar component dominates.

We also allow for an overall constant but non-zero velocity anisotropy $\beta_z$ in the model. The model parameters $(\Upsilon_{1,\text{tot}}^\text{dyn}, \beta_z)$ that fit the $v_{\text{rms}}$ data best are found using a $\chi^2$-fit and are demonstrated in Figure 6.

For $\beta_z$ we imposed the fitting limits $\beta_z \in [-0.5, +0.5]$. While the outer parts of galaxies often show radially biased velocity anisotropy up to $\sim 0.5$ (from dynamical modelling of observed elliptical galaxies, e.g., Kronawitter et al. (2000)) and cosmological simulations (e.g., Diemand et al. 2004; Fukushige & Makino 2001), the centers of galaxies are near-isotropic or have negative velocity anisotropy (Gebhardt et al. 2003). Only in extreme models (e.g., around in-spiralling supermassive black holes, e.g., Quinlan & Hernquist 1997) velocity anisotropies as low as $\sim -1$ have been found.

The best fit in Figure 6 however strives to very negative $\beta_z$ to be able to reproduce the deep central dip in the $v_{\text{rms}}$ curve.\footnote{Without limiting the fitting range, the best fit would be an unrealistically low $\beta_z \sim -2$.} But $\beta_z = -0.5$ is not even a remotely agreeable fit and lower anisotropies are not to be expected or realistic. We also tested radial profiles for $\beta_z(R)$ of the form proposed by Baes & van Hese (2007), which was however equally unable to reproduce the data. We conclude that this is due to the well-known degeneracy between anisotropy and mass profile and the mass-follows-light model is not a good representation of the mass distribution in J1331’s inner regions.

4.3.3 JAM with increasing mass-to-light ratio

In Section 4.2.3 we found from lensing constraints that the light distribution might drop faster with radius than the mass distribution. This corresponded to a radially increasing total mass-to-light ratio. As velocity anisotropy alone cannot explain the observed kinematics in a simple mass-follows-light model, we now allow for a mass-to-light ratio gradient in the JAM modelling. We therefore generate a mass model from the light distribution in Table 3 by assigning each of the five Gaussians in the MGE its own total mass-to-light ratio $\Upsilon_{1,\text{tot},i}$, and replace the total luminosity in Equation (13), $L_i$, with the Gaussians total mass $M_i = \Upsilon_{1,\text{tot},i} \times L_i$. We treat the five $\Upsilon_{1,\text{tot},i}$ as free fit parameters and only require that $\Upsilon_{1,\text{tot},i} \geq \Upsilon_{1,\text{tot},j}$ when the corresponding $\sigma_i \geq \sigma_j$ to ensure that the overall mass-to-light ratio is increasing with radius.

Figure 7b shows the best-fitting (projected local) mass-to-light ratio profile, which rises from $\Upsilon_{1,\text{tot}} = 2.53$ in the center and approaches a value of $\Upsilon_{1,\text{tot}} = 7.60$ outside of the fitted region at $R' > 3''$. The central mass-to-light ratio is in agreement with the mass-to-light ratio $\Upsilon_{1,\text{tot}}^{\text{obs}} = 2.5 \pm 0.6$, which was however equally unable to reproduce the data. We conclude that this is due to the well-known degeneracy between anisotropy and mass profile and the mass-follows-light model is not a good representation of the mass distribution in J1331’s inner regions.

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given in Table 7 based on the results of Treu et al. (2011) assuming a stellar population with a Chabrier (2003) IMF (see also Section 5.2). When assuming that galaxy bulges are in general older and redder in the center, i.e., $\Upsilon_{1,\ast}$ is more likely to drop with radius than rise, the strong increase of $\Upsilon_{1,\text{tot}}(R')$ might be due to a strong contribution of DM in J1331.

Figure 7a shows that the best-fitting model nicely reproduces the central dip in the $v_{\text{rms}}$ curve, even though it has difficulties fitting the drop around $R' \sim 4'$. The latter is because we only allowed the $\Upsilon_{1,\text{tot}}(R')$ to rise. A slight drop could be expected when the reddish bulge turns into the bluish disk and the contribution of the stellar component becomes less due to a lower $\Upsilon_{1,\ast}$ for younger and bluer populations. Corresponding fitting attempts with the matter model at hand were however unsuccessful: Leaving all five $\Upsilon_{1,\text{tot},i}$ free to over-fitting in the central regions of J1331, while not allowing for sufficient flexibility further out at $R' \gtrsim 4'$ to properly model the transition from bulge to disk (because four of the five $\sigma_i$ in the light MGE in Table 3 are $< 1.2''$).

For the inner regions the model with rising $\Upsilon(R')$ seems however to be a very good model: In Figure 7b we overplot the enclosed mass profile with the Einstein mass $M_{\text{Ein}} = (7.77 \pm 0.33) \times 10^{10} M_\odot$ at the Einstein radius found from lensing in Table 5. The agreement between the Einstein mass and the independently found $M(< R_{\text{Ein}}) = 7.49 \times 10^{10} M_\odot$ from dynamical modelling is striking.

4.4 JAM with an NFW dark matter halo

The modelling attempts in the previous sections suggest that J1331's mass distribution could be more roundish in the inner regions and more massive at larger radii than expected from the distribution of stars alone. A DM halo in addition to the stellar component could explain these findings.

4.4.1 Modelling and priors

We proceed by modelling the mass distribution with (i) a stellar component, which we get from the light MGE in Table 3 (deprojected to the intrinsic $\nu(R,z)$ using the fixed inclination angle $i = 70^\circ$ in Table 1) times a constant stellar mass-to-light ratio $\Upsilon_{1,\ast}$, and (ii) a spherical NFW DM component (see Section 3.3.4) with halo scale length $r_s$ and circular velocity $v_{200}$ at the virial radius as free parameters. In the JAM modelling we use a 10-Gaussian MGE fit to the classical NFW profile from Equation (28).

The full set of fit parameters is $(\Upsilon_{1,\ast}, r_s, v_{200}, \beta_z)$, where $\beta_z$ is again the constant velocity anisotropy parameter. We will investigate this parameter space with a Monte Carlo Markov Chain (MCMC; using code by Foreman-Mackey et al. 2013).

As we are particularly interested in the disentanglement of DM and stellar matter in the inner regions (see Section 1), we restrict the $v_{\text{rms}}$ fit to a region $R' \lesssim 3.5''$, approximately within the effective half-light radius $R_{\text{eff}} = 2.6''$. The constraints on a DM halo just from this data might be weak. To guide the fit towards a realistic NFW halo shape, we therefore impose several priors on the NFW halo.

Dutton et al. (2010) give a relation for halo vs. stellar mass for late-type galaxies. Using the stellar mass estimate for J1331 from Treu et al. (2011), $m_\ast = (1.06 \pm 0.25) \times 10^{11} M_\odot$ (with generous error; see also Table 7) for the Chabrier IMF estimate, we find $v_{200} = (202^{+44}_{-33})_{-13}$. The first error is due to the 2\sigma scatter in the relation by Dutton et al. (2010). The second error is the propagated error due to the uncertainty in the stellar mass. We use this as a rough estimate for the halo of J1331 and as Gaussian prior on $v_{200}$,

$$p(v_{200}) = \mathcal{N}(200 \text{ km s}^{-1}, 40 \text{ km s}^{-1}).$$

We also use the concentration vs. halo mass relation by Macciò et al. (2008) in Equation (29) as a prior on the concentration, i.e.

$$p(\log c_{200} | v_{200}) = \mathcal{N}(\log c_{200}(M_{200}), 0.105).$$

For the velocity anisotropy parameter $\beta_z$ we will again employ a uniform prior

$$p(\beta_z) = \mathcal{U}(-0.5, +0.5)$$

to exclude very unrealistic anisotropies. The full prior used is then

$$p(\Upsilon_{1,\ast}, r_s, v_{200}, \beta_z) = \frac{1}{\ln (10 r_s)} p(\log c_{200} | v_{200}) \times p(v_{200}) \times p(\beta_z),$$

where the factor $1/\ln (10 r_s)$ is the Jacobian of the transformation from the halo parameters $(v_{200}, \log c_{200})$ to the fit parameters $(v_{200}, r_s)$.

We also include the Einstein mass $M(< R_{\text{Ein}})$ with a 10% error as an additional constraint in the fit.

4.4.2 Best-fitting JAM model

Figure 8 shows the posterior probability distribution (pdf) of the fit sampled with an MCMC. Overplotted are also the priors used to constrain the NFW halo. The mean parameters are summarized in Table 6. We find that the best-fitting NFW halo strives to be more massive and with a higher concentration (due to a smaller $r_s$) than proposed by the priors. The model also prefers very negative velocity anisotropies. Both, the high halo concentration and low $\beta_z$, are needed to reproduce the central dip of the $v_{\text{rms}}$ curve. Figure 9 illustrates the range of best-fitting models according to the extent of the pdf. The models fit the $v_{\text{rms}}$ data in the inner regions quite well (Figure 9a) and are also consistent with the Einstein mass (see Figure 9b). The extrapolation of the model to larger radii however overestimates the data, does not exhibit a drop around $\sim 6''$ at all and seems to be therefore overall too massive.

4.4.3 Rotation curve

We generate a rotation curve from the best-fitting mean model in Table 6, whose $v_{\text{rms}}$ curve is shown in the first...
Figure 8. Posterior probability distribution (pdf) sampled with a Monte Carlo Markov Chain (MCMC) (red dots and histograms) for a JAM model fitted to the stellar $v_{\text{rms}}$ data, with NFW halo, parametrized by $r_s$ and $v_{200}$, a stellar mass distribution generated from the I-band MGE in Table 3 and a constant stellar mass-to-light ratio $\Upsilon_{I,*}$, and constant velocity anisotropy $\beta_z$. Shown are also the priors used for J1331’s NFW halo, $N(200 \text{ km s}^{-1}, 40 \text{ km s}^{-1})$ (green, see Equation (34)) and the concentration vs. halo mass relation by Macciò et al. (2008) from Equation (29) in terms of $v_{200}$ vs. $r_s$ with 1$\sigma$ scatter (blue, see Equation (35)). We find slight covariances between $\Upsilon_{I,*}$, $r_s$ and $\beta_z$: The smaller the DM contribution in the center (i.e., the larger $\Upsilon_{I,*}$), the less concentrated is the halo (i.e., the larger $r_s$) and the more velocity anisotropy is needed to reproduce the central $v_{\text{rms}}$ dip. As the effect of $v_{200}$ is mostly at larger radii, this parameter does not show any covariances, but is also mostly constrained by the prior. The MCMC samples are colour coded according to their probability (darker red for higher probability); the sample point with the highest probability is marked by a black diamond. The black cross is the mean of the distribution and the ellipses are derived from the covariance matrix of the MCMC samples and correspond approximately to 1$\sigma$ (black solid ellipse) and 2$\sigma$ (black dotted ellipse) confidence. The histograms of the marginalized 1D distributions are overplotted by the mean (black solid lines) and 1$\sigma$ error (black dashed lines), whose values are also quoted in the figure and in Table 6. The grey diamonds mark a random sub-selection of 12 samples; the corresponding models are shown in Figure 9.

panel of Figure 10. Following the procedure in Section 3.3.3, we find the rotation curve by fitting the rotation parameter $\kappa'$ to the symmetrized $v_{\text{rot}}$ data within $R' = 3.5''$. The best fit with $\kappa' = 0.76$ is given in the second panel of Figure 10. The third panel shows the dispersion that follows from $\sigma = \sqrt{v_{\text{rms}}^2 - v_{\text{rot}}^2}$. Our assumptions for $\kappa(R)$ nicely reproduce a $v_{\text{rot}}$ model with counter-rotating core. Although we fitted $v_{\text{rot}}$ only to the inner regions, the extrapolation to large radii matches the data also very well.

While the dispersion $\sigma$ in the center fits by construction quite good, the extrapolated dispersion is much larger than the data. We would expect the disk to be rotationally...
Enclosed mass profiles for the best-fitting models.

Figure 9. JAM model including an NFW halo and constant velocity anisotropy fitted to the stellar \(v_{\text{rms}}\) data (blue solid dots) within \(\sim 3.5''\) and the Einstein mass (red solid dot). The 12 lines shown correspond to 12 models randomly drawn from the pdf (marked as grey diamonds in Figure 8) and their range demonstrates how tight the modelling constraints are. The mean and standard deviation of the pdf, i.e., the "best fit" parameters, are given in Table 6. Panel (a): At \(R' \lesssim 3.5''\) the symmetrized \(v_{\text{rms}}\) data used in the fit (solid blue points) is shown together with the best-fitting \(v_{\text{rms}}\) models (red solid lines). At larger radii the non-symmetrized data (open blue dots) is compared to an extrapolation of the best-fitting models using the surface brightness MGE for the outer regions from Figure 2b (red dashed lines). Panel (b): Shown is the projected enclosed mass profile of the total mass (green), and separately the contribution of the stellar mass (yellow, again generated from the MGE in Table 3) and DM (grey). At the Einstein radius \(R_{\text{Ein}}\) (red dotted line) the Einstein mass \(M_{\text{Ein}}\) is overplotted with a 10% error, which was also included in the fit as additional constraint. Overplotted is also the effective half-light radius (black dotted line) and the blue dashed line marks the radius within which the data and model were fitted.

Table 6. Summary of the best-fitting parameters of the JAM model with NFW halo and constant velocity anisotropy, fitted to the \(v_{\text{rms}}\) data within \(\sim 3.5''\) and the Einstein mass \(\pm 10\%\). These estimates correspond to the mean and standard deviation of the pdf in Figure 8. The halo mass and concentration are calculated from the best-fitting \(v_{\text{rms}}\) and \(v_{200}\).

| Parameter                              | Value       |
|----------------------------------------|-------------|
| stellar I-band mass-to-light ratio     | 4.2 ± 0.2   |
| velocity anisotropy                    | -0.4 ± 0.1  |
| NFW halo scale length                  |             |
| NFW halo virial velocity \(v_{200}\) [km s\(^{-1}\)] | 240 ± 40    |
| NFW halo concentration \(c_{200}\)    | 8 ± 2       |
| NFW halo mass                          | 5 ± 2       |

supported and therefore have a low velocity dispersion. Especially dispersions as high as \(\sim 200\) km s\(^{-1}\) are more likely to be observed in the pressure supported bulges of galaxies. There might be something unexpected with the \(\sigma\) measurements around \(\sim 5''\), but at large radii the best-fitting model NFW halo is simply too massive.

4.4.4 Further tests and discussion

We also fitted a model with a cored logarithmic DM halo. The cored halo models are in general slightly less massive than the NFW halo and therefore fit the outer regions of J1331 better. However, the density profile of the cored halo as well as the \(I\)-band light distribution within the plane drop as \(\rho(r) \propto r^{-2}\). There is therefore a strong degeneracy between the stellar mass and the DM. Overall, we were not able to obtain tight constraints on the cored logarithmic halo.

As we only fitted the halo models to the inner regions, it is not surprising that they do not fit the kinematics at larger radii. A fit to all nine available \(v_{\text{rms}}\) data points would force the DM halo to be less massive. But with decreasing DM contribution in the inner regions the model approaches the mass-follows-light model in the center that we already ruled out in Section 4.3.2. Allowing for free \(\Upsilon_{I^*}(R')\), \(\beta_z(R')\), and more flexible \(\rho_{\text{halo}}(r)\) profiles, which would be the reasonable next step, would over fit the data. Without further priors on the stellar \(\Upsilon_{I^*}(R')\) or more data points, we can make only the following statement: A model with constant \(\Upsilon_{I^*} = 4.2 ± 0.2\), moderately tangential \(\beta_z = -0.4 ± 0.1\) and a spherical and massive DM component with high concentration \((c_{200} = 8 ± 2)\) can explain the central kinematics of J1331 very well. We have however ruled out that in this case the DM halo will follow an NFW halo profile at both small and large radii.

We will also discuss the kinematics at larger radii in more depth in the discussion Section 5.3.

5 DISCUSSION AND CONCLUSION

We have presented different dynamical models for the central region of J1331. Some of them capture the observed kinematics, but none of them work at both small and large radii. In the following we try to resolve some of the am-
The different components with angular momenta oriented in opposite directions This suggests a process in J1331’s past in which two components were involved. Some of the ambiguities in recovering J1331’s matter distribution could be resolved by learning more about stellar populations with different IMFs in J1331. In particular, a sophisticated guess for the stellar mass-to-light ratio in the bulge could be compared to our very reliable measurement of the total mass-to-light ratio inside the Einstein radius \( \Upsilon_{\text{tot}} \). This would then either support or contradict the presence of a significant amount of DM in the bulge. Traditional choices for the IMF are the bottom-heavy IMF by Salpeter (1955), \( \xi(m) \propto m^{-2.35} \) with \( x = 2.35 \), where \( \xi(m) \, dm \) is the number of stars with mass \( m \) in \( [m, m + dm] \), and the IMFs by Kroupa (2002) and Chabrier (2003), which are in agreement with each other and predict less low-mass stars. In the following we discuss why we think—based on our results and previous analyses—that J1331’s bulge has an IMF slightly less bottom-heavy than the Salpeter-like IMF.

(i) Indications for a slightly less bottom-heavy Salpeter-like IMF in J1331’s bulge:

Ferreras et al. (2013) found a relation between the central stellar velocity dispersion \( \sigma_0 \) in early-type galaxies and the IMF slope \( x \), where a higher \( \sigma_0 \) suggests a more bottom-heavy IMF. For a unimodal (Salpeter-like) IMF and \( \sigma_0 \approx 200 \, \text{km s}^{-1} \) in J1331 (see Figure 1d), this relation predicts...
Table 7. Total I-band luminosity, stellar mass, and mass-to-light ratio, calculated from the I-band AB magnitudes and stellar masses found for J1331’s bulge and disk by Treu et al. (2011) (their table 2) for comparison with this work. The transformation from AB magnitudes to the Johnson-Cousins I-band used the relation $I_{\text{mag}} = I_{\text{ABmag}} - 0.309$ from Frei & Gunn (1994) (their table 2). For the conversion from apparent magnitude to total luminosity the redshift $z = 0.113$ Brewer et al. (2012) was turned into a luminosity distance using the WMAP5 cosmology by Dunkley et al. (2009).

|                | Chabrier IMF | Salpeter IMF |
|----------------|-------------|-------------|
|                | $L$ [10^{10}L_\odot] | $M_\ast$ [10^{10}M_\odot] | $\Upsilon_1^{\text{chab}}$ |
| bulge          | 3.10 ± 0.15 | 7.8 ± 1.8 | 2.5 ± 0.6 |
| disk           | 2.35 ± 0.11 | 2.9 ± 0.7 | 1.2 ± 0.3 |
| total          | 5.45 ± 0.19 | 10.6 ± 1.9 | 19.7 ± 3.9 |

$x \approx 2.33$, which is close to the standard Salpeter slope, also supported by Spiniello et al. (2014). When assuming a bimodal (Kroupa-equivalent-like) IMF, Ferreras et al. (2013) predict $x \approx 2.85$ for J1331’s central velocity dispersion. This is more bottom-heavy than the standard Kroupa (2002) IMF. Overall, the central velocity dispersion suggests a rather bottom-heavy IMF in J1331’s bulge and therefore large stellar mass-to-light ratio.

Treu et al. (2011) estimated J1331’s stellar bulge mass given a Salpeter IMF and measured the I-band AB magnitude of the bulge. Transformed to a stellar I-band mass-to-light ratio, their results would correspond to $\Upsilon_{1,\ast}^{\text{chab}} = 4.7 \pm 1.2$ (see Table 7). This is not too far from $\Upsilon_{1,\ast} = 4.2 ± 0.2$ (see Table 6), which we found when including an NFW halo in the JAM modelling.

(ii) Indications for and arguments against a Chabrier-like IMF in J1331’s bulge:

When Treu et al. (2011) assumed a Chabrier IMF, their result translates to $\Upsilon_{1,\ast}^{\text{chab}} = 2.5 ± 0.6$ (see Table 7). In Section 4.3.3, we created a dynamical model from only the surface brightness distribution and an increasing mass-to-light ratio profile without additional DM halo and without velocity anisotropy. We found that such a model would be perfectly consistent with the Einstein mass, predict a total $\Upsilon_{1,\ast}(R \sim 6\text{''})$—being consistent with the Chabrier IMF estimate by Treu et al. (2011)—and rise quickly to $\Upsilon_{1,\ast}(R \gtrsim R_{\text{Ein}}) \gtrsim 0$.

This rise in $\Upsilon_{1,\ast}(R')$ could be either due to a cuspy DM halo (see Section 4.4) or a very strong gradient in $\Upsilon_{1,\ast}$ (see Section 5.1). However, we rule out that a DM cusp is the sole reason because a cuspy and therefore overall massive DM halo does not match the kinematics in J1331’s outer regions. We also rule out that a very strong $\Upsilon_{1,\ast}$ gradient is the only reason, because—as mentioned in Section 5.1—photometry did not reveal the clear existence of a blue population in the very center of J1331’s bulge. Also, our modelling attempts allowing for velocity anisotropy (Sections 4.3.2 and 4.4) suggest that we do need some moderate $\beta \gtrsim 0$ to explain the central $v_{\text{rms}}$ dip. And lastly—as laid out in the previous paragraph—J1331’s central velocity dispersion suggests a more bottom-heavy IMF. Overall it is therefore not very likely that the central regions of J1331 have such a low $\Upsilon_{1,\ast}^{\text{chab}} \sim 2.5$.

(iii) Arguments against an IMF more bottom-heavy than the Salpeter IMF in J1331’s bulge:

We also compare our results from Section 4.4 with the study by Dutton et al. (2013). They found that the bulge of J1331 has an IMF more bottom-heavy than the Salpeter IMF. Our fitting attempt—using more data within $\sim 3.5\text{''}$ than Dutton et al. (2013) in Section 4.4 gave $\Upsilon_{1,\ast} = 4.2 ± 0.2$ as best fit (see Table 6), which indicates a less bottom-heavy IMF than the Salpeter IMF. In Section 5.3, we will argue why we do not think that the Dutton et al. (2013) model is a good model for the central regions of J1331.

5.3 On J1331’s kinematics

Overall, the kinematics of the merger remnant J1331 are peculiar. In particular, there are two features in the $v_{\text{rms}}$ curve that are hard to explain with standard modelling techniques. The first feature, the deep central $v_{\text{rms}}$ dip, was studied in detail in this work. The second feature, the drop and rise in $v_{\text{rms}}$ around $R \sim 6\text{''}$, is even harder to explain; below we will speculate about possible reasons that could cause such a signature.

(i) The central $v_{\text{rms}}$ dip within $R' \lesssim 1\text{''}$:

First, we will compare our modelling results with the modelling results by Dutton et al. (2013) within $R_{\text{Ein}}$. Dutton et al. (2013) fitted a stellar mass model and NFW halo to (i) the Einstein mass and (ii) gas kinematics at larger radii $\gtrsim 8\text{''}$. Figure 11 compares the circular velocity curve found by Dutton et al. (2013) with a mass-follows-light model scaled to fit our Einstein mass (by multiplying the light distribution in Table 3 by $\Upsilon_{1,\ast}^{\text{chab}} = 5.56$, analogous to Figure 4a). Within $0.5 < R < 5\text{''}$ they agree with each other.

The models in this work used more than just the Einstein mass to constrain the matter distribution at small radii. The lens mass model constrained also the shape of the mass distribution within the lensing image configuration at $R_{\text{Ein}} \sim 1\text{''}$. The dynamical models used stellar kinematics inside $R' \sim 3.5\text{''}$. We compare the lens mass model’s trice (for $\alpha = 1.0 ± 0.1$) with the NFW JAM model (Table 6) in Figure 11 as well. Within and around $R_{\text{Ein}}$ they are consistent with each other, even though they were independently derived. They do not agree with the mass-follows-light-like result by Dutton et al. (2013) and in Section 4.3.2 we showed that “mass-follows-light” is not a good model for J1331.

Because we used more data constraints in the center than Dutton et al. (2013), we think that our model for J1331’s bulge is more reliable. In conclusion, we suspect that the most likely model for J1331’s central bulge is a moderate DM contribution in the center (Section 4.4.2) with some tangential anisotropy (Sections 4.3.2 and 4.4, which would be also consistent with the counter-rotation in the bulge) and an overall $\Upsilon_1$ in the bulge which is slightly lower than $\Upsilon_{1,\ast}$.
that of a Salpeter-like IMF (Section 5.2). Different stellar populations inside the bulge due to the merger (Section 5.1) with different $\Upsilon_*$ could add to an overall rising $\Upsilon_{\mathrm{tot}}(R')$ profile (Sections 4.2.3 and 4.3.3).

(ii) The drop and rise of the $v_{\text{rms}}$ curve around $R' \sim 6''$: The drop in $v_{\text{rms}}$ around $R' \sim 4''$ (Figure 1d) is most likely due to the transition from red bulge to blue disk (compare bulge size in Figures 1a and 1b). A mix of different stellar populations in the disk could make the modelling difficult: The smooth light distribution was derived from the F814W filter and is therefore dominated by older stars, while the measured light-weighted stellar kinematics in the disk are dominated by luminous young stars with their lower velocity dispersion. As the merger could have caused a warp in J1331’s disk, it is possible that bulge and disk have different inclination angles and a kinematic twist. The latter could have lead to a misalignment of the long-slit and the galaxy’s kinematic major axis at larger radii, therefore to measurements of lower $v_{\text{rms}}$ and consequently to a stronger underestimation of the true $v_{\text{circ}}$, which would add to the drop in $v_{\text{rms}}$.

Around $R' \sim 7''$ the rotation curve and dispersion show some wiggles which lead to a spontaneous rise of the $v_{\text{rms}}$. As the spiral arms with their non-circular motions and patchy star-forming regions cross the major axis around this radius, we suspect they cause this disturbance of the axisymmetric kinematics.

(iii) The profile of the DM halo at $R' \geq 5''$: The DM halo should start to dominate the kinematics at larger radii. Dutton et al. (2013), who fitted an NFW halo to the gas kinematics in the outer regions, found lower halo masses ($v_{\text{circ},\text{halo}}(5'') \sim 120$ km s$^{-1}$ according to their Figure 2) than we did ($v_{\text{circ},\text{halo}}(5'') \sim 200$ km s$^{-1}$, Figure 11). As we did not fit the outer regions and only used a prior for $v_{200}$, their result in this regime is more reliable. Given our findings that an NFW halo does not fit the kinematics at both small and large radii, we suspect that the true halo has a profile that deviates strongly from an NFW halo, possibly as a result of the merger.

All of these speculations should be easily testable with 2D kinematics.

5.4 Future work
J1331’s merging history and peculiar kinematics make it a valuable and exiting target to study merger remnants and a challenge for dynamical modelling techniques. We found however that the existing data alone—photometry and major axis kinematics—is not sufficient to resolve all the ambiguities we encountered in our modelling.

The main future work would be therefore getting high-resolution integral-field spectroscopy for J1331. High spatial resolution would be required to clearly identify J1331’s presumably complex kinematic structure. High spectral resolution would be important to be able to reliably measure the low velocity dispersion in the outer regions of J1331.

Specifically 2D kinematics should help to answer the following questions: Is the drop in $v_{\text{rms}}$ around $R' \sim 3–6$ kpc real? Did the long slit spectrograph maybe miss the major axis of the disk? And most importantly: Are the kinematics asymmetric? Is it possible that there even exists a kinematic twist due to the merger in J1331’s past? In the latter two cases we would need to apply non-axisymmetric Jeans models to J1331 as the assumption of axisymmetry of this work would not be valid anymore.

Furthermore, learning more about different stellar populations in J1331 would lead to valuable constraints for the modelling. While a quick investigation of the photometric colour profile did not reveal obvious colour gradients in J1331’s bulge, there could be still stellar $\Upsilon_*$ variations due to age or metallicity differences. Existing major axis spectroscopy and/or future IFU data could be employed (i) to investigate absorption line indices to confirm (or contradict) the existence of $\Upsilon_*$, gradients and (ii) to perform stellar population analyses to constrain $\Upsilon_*$, reliably and independently of kinematics.

Future modelling approaches should fit dynamics (stellar and gas kinematics) simultaneously with the gravitational lensing (image positions, shape and even flux ratios) in a similar fashion to Barnabè et al. (2012). To also model the extent, shape and flux of the lensing images, the method by Treu & Koopmans (2004); Warren & Dye (2003) could be employed, which models the surface brightness distribution of the images and source on a pixelated grid. For this to work, a good model for the galactic extinction would be needed—but 2D spectroscopy could also help with this.

All of the above would lead to a much better understanding of J1331’s structure and mass distribution and therefore answer questions on how mergers might modify spiral galaxies.

5.5 Summary
We constrained the matter distribution of the massive spiral galaxy J1331, which has a large counter-rotating core,
probably due to a merger in its past, and acts as a strong gravitational lens for a background source. We used two independent methods to model J1331: gravitational lensing and dynamical Jeans modelling. We focused on the bulge region of J1331 to complement previous studies of J1331 by Brewer et al. (2012) and Dutton et al. (2013). The mass constraints from lensing and dynamics agree very well with each other within $R_{\text{eff}}$.

In our lensing approach we fitted a scale-free galaxy model to the lensing image position. This constrained the Einstein radius to within 2% [$R_{\text{Ein}} = (0.91 \pm 0.02)'' = (1.83 \pm 0.04)$ kpc], and the Einstein mass to within 4% [$M_{\text{Ein}} = (7.8 \pm 0.3) \times 10^{10} M_\odot$], consistent with results by Brewer et al. (2012).

A MGE fit to J1331’s surface brightness in the F814W filter in HST imaging by Treu et al. (2011) helped us determining the effective radius, $R_{\text{eff}} \simeq 2.6'' = 5.2$ kpc, and total $I$-band luminosity of the galaxy, $L_I,_{\text{tot}} \simeq 5.6 \times 10^{10} L_\odot$.

Axisymmetric JAM modelling allowed a comparison between model predictions for the second velocity moment given a tracer and mass distribution and the observed stellar kinematics from major axis long slit spectroscopy by Dutton et al. (2013). The independent JAM model of the lens mass model was consistent with observed kinematics within $R_{\text{eff}}$. We also fitted mass models with and without NFW halo to the stellar kinematics within $R' = 3.5$ kpc. From this we deduced that a mass-follows-light model (even with velocity anisotropy) is not a good model for J1331’s inner regions. This ruled out the previous findings of Dutton et al. (2013) for J1331’s bulge. We discussed that, to describe the observed stellar kinematics, we most likely require a moderate contribution of a DM halo already in the bulge, moderate tangential velocity anisotropy, $\beta_z \sim -0.4 \pm 0.1$, and possibly even a varying stellar mass-to-light ratio, which could be the result of the previous merger event. We argue that we expect the total stellar mass-to-light ratio within the bulge to be $T^{1+}_{I,\text{eff}} \sim 4.2 \pm 0.2$, which is slightly less bottom-heavy than a Salpeter IMF ($T^{1+}_{I,\text{eff}} \sim 4.7$). We also showed that it is possible to construct a model which includes the counter-rotating core and fits the rotation curve at large radii.

While both our independent mass models are consistent with each other within $\sim R_{\text{eff}}$, they do not describe the data at large radii very well. We speculate how a merger could have modified the kinematic structure and/or mass distribution of J1331. To resolve the ambiguities in J1331’s mass distribution two-dimensional kinematic maps of J1331 from integral-field unit spectroscopy are needed.

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