Study of central exclusive $\pi^+\pi^-$ production in proton-proton collisions at $\sqrt{s} = 5.02$ and 13 TeV

CMS Collaboration

CERN, 1211 Geneva 23, Switzerland

Abstract  Central exclusive and semiexclusive production of $\pi^+\pi^-$ pairs is measured with the CMS detector in proton-proton collisions at the LHC at center-of-mass energies of 5.02 and 13 TeV. The theoretical description of these non-perturbative processes, which have not yet been measured in detail at the LHC, poses a significant challenge to models. The two pions are measured and identified in the CMS silicon tracker based on specific energy loss, whereas the absence of other particles is ensured by calorimeter information. The total and differential cross sections of exclusive production are measured as functions of invariant mass, transverse momentum, and rapidity of the $\pi^+\pi^-$ system in the fiducial region defined as transverse momentum $p_T(\pi) > 0.2$ GeV and pseudorapidity $|\eta(\pi)| < 2.4$. The production cross sections for the four resonant channels $f_0(500)$, $\rho^0(770)$, $f_0(980)$, and $f_2(1270)$ are extracted using a simple model. These results represent the first measurement of this process at the LHC collision energies of 5.02 and 13 TeV.

1 Introduction

The central exclusive production (CEP) process has been studied for a long time from both theoretical [1–7] and experimental [8–18] perspectives. In this process, both protons remain intact in the collision and a central system is produced. The process is referred to as exclusive when no particles other than the central system are produced. If one or both protons dissociate into a forward diffractive system, the process is called semiexclusive production. Various central systems can be produced in this process, like $\pi^+\pi^-$, $K^+K^-$, and $4\pi$. In this paper, the $\pi^+\pi^-$ central system is measured. At the CERN LHC energies, the two dominant mechanisms of $\pi^+\pi^-$ production via CEP are double pomeron exchange (DPE) and vector meson photoproduction (VMP), which are illustrated by the diagrams shown in Fig. 1. The pomeron ($P$) is a color singlet object introduced to explain the rise of the inelastic cross section at high collision energies [19,20]. The quantum numbers of the pomeron constrain the possible central systems in DPE processes, whereas the photon exchange restricts the central system in VMP processes. By functioning as a quantum number filter, the CEP process is suitable to study low-mass resonances, which would be difficult to study otherwise. Furthermore, DPE processes are also suitable to search for glueballs (bound states of gluons without valence quarks), because they provide a gluon-rich environment [21,22]. Another process that could contribute to the same final state is the two-photon fusion $\gamma\gamma \rightarrow \pi^+\pi^-$, which is expected to have a much smaller cross section than DPE and VMP processes and gives a negligible contribution [23].

The DPE process of pion pair production has two sub-categories: continuum and resonant production. In the case of continuum production, the pion pair is directly produced; thus the pairs have a nonresonant invariant mass spectrum. Resonant production means that an intermediate meson resonance is produced centrally, which manifests itself as a peak in the invariant mass distribution of the pion pair. Since the pomeron is a Regge trajectory running over states with quantum numbers $J^{PC} = \{0^{++}, 1^{++}, 2^{++}, \ldots \}$ and $I^G = 0^+$, the resonance is restricted to have $J^{PC}_G = \{0^{++}, 2^{++}, 4^{++}, \ldots \}$ and $I^G = 0^+$, where $J$ is the total angular momentum, $I$ is the isospin, $P$ is the parity, $C$ is the charge parity, and $G = C (-1)^I$. The known particles [24] satisfying these criteria are the $f_0$, $f_2$, $\chi_{c0}$, $\chi_{c2}$, $\chi_{b0}$, and $\chi_{b2}$ resonances. The cross section for DPE ($\sigma^{DPE}_{\pi^+\pi^-}$) can be calculated from the amplitude of continuum ($A^{DPE,C}_{\pi^+\pi^-}$) and resonant ($A^{DPE,R}_{\pi^+\pi^-}$) production as

$$\sigma^{DPE}_{\pi^+\pi^-} \propto |A^{DPE,C}_{\pi^+\pi^-} + A^{DPE,R}_{\pi^+\pi^-}|^2. \quad (1)$$

Interference terms between the continuum and resonant production channels must be included to describe the observed spectra and to measure the cross sections for resonances.
In VMP, one of the protons emits a virtual photon, which fluctuates into a quark-antiquark bound state and scatters from the proton via the pomeron exchange. The quantum numbers of the possible resonances are constrained by the quantum numbers of the pomeron and the photon \( J^{PC} = 1^{--} \), leading to mesons with odd spin and the following quantum numbers \( J^{PC} = \{1^{--}, 3^{--}, \ldots \} \). Resonances satisfying these conditions are \( \rho, \omega, \phi, J/\psi, \psi(2S), \) and \( Y \), but only the \( \rho^0 \rightarrow \pi^+\pi^- \) decay has a significant branching fraction, since decays in this channel are strongly suppressed in the case of \( \phi, J/\psi, \psi(2S), \) and \( Y \) according to the Okubo–Zweig–Iizuka rule \([25–27]\) and in the case of \( \omega \) because of G-parity conservation \([28]\).

This paper presents measurements of exclusive and semiexclusive \( \pi^+\pi^- \) total and differential cross sections as functions of invariant mass \( m(\pi^+\pi^-) \), transverse momentum \( p_T(\pi^+\pi^-) \), and rapidity \( y(\pi^+\pi^-) \) of the pion pair, in a fiducial region defined by single pion transverse momentum \( p_T(\pi) > 0.2 \text{ GeV} \) and single pion pseudorapidity \( |\eta(\pi)| < 2.4 \). Because the outgoing protons are not tagged in this measurement, there is a residual contribution from semiexclusive production with all dissociation products outside the \( |\eta| > 4.9 \) range. In the following, the exclusive and the residual semiexclusive contribution together will be referred to as central exclusive production. The data were recorded by CMS with beam conditions ensuring a small probability of multiple pp collisions in the same bunch crossing (pileup) in August 2015 at a center-of-mass energy of 13 TeV with luminosity 258 \( \mu \text{b}^{-1} \) and in November 2015 at 5.02 TeV with a luminosity of 522 \( \mu \text{b}^{-1} \). The average number of pp collisions in a bunch crossing was around 0.3–0.5 for the 5.02 TeV and around 0.5 for the 13 TeV data sets.

2 The CMS detector

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter. Within the solenoid volume are a tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections, covering the \( |\eta| < 3.0 \) region. Forward calorimeters extend the \( \eta \) coverage provided by the barrel and endcap detectors. Muons are measured in gas-ionization detectors embedded in the steel flux-return yoke outside the solenoid.

The silicon tracker measures charged particles within the range \( |\eta| < 2.5 \). It consists of 1440 silicon pixel and 15 148 silicon strip detector modules and is located in the 3.8 T solenoid field. Three pixel barrel layers (PXB) are situated at radii of 4.4, 7.3, and 10.2 cm; PXB also has two pixel endcap disks (PXB). The strip tracker consists of the innermost tracker inner barrel (TIB) and the tracker inner disks (TID), which are surrounded by the tracker outer barrel (TOB). It is completed by endcaps (TEC) on both sides. The barrel part of the strip tracker has a total of 10 layers at radii from 25 to 110 cm, whereas the endcap of the strip tracker consists of 12 layers. For charged particles with \( p_T < 1 \text{ GeV} \) and \( |\eta| < 1.4 \), the track resolutions are typically 1–2\% in \( p_T \). and 90–300 and 100–350 \( \mu \) for the transverse and longitudinal impact parameters, respectively \([29]\). The tracker provides an opportunity to identify charged particles with \( 0.3 < p < 2 \text{ GeV} \) based on their specific ionization in the silicon detector elements \([30]\).

The ECAL consists of 75 848 lead tungstate crystals, which provide coverage in \( |\eta| < 1.479 \) in the barrel region and \( 1.479 < |\eta| < 3.0 \) in the two endcap regions.

The barrel and endcap sections of the HCAL consist of 36 wedges each and cover the \( |\eta| < 3.0 \) region. In the region \( |\eta| < 1.74 \), the HCAL cells have widths of 0.087 in \( \eta \) and
0.087 radians in azimuth ($\phi$). In the $\eta$-$\phi$ plane, and for $|\eta| < 1.48$, the HCAL cells map onto $5 \times 5$ ECAL crystal arrays to form calorimeter towers projecting radially outwards from close to the nominal interaction point. At larger values of $|\eta|$, the towers are larger and the matching ECAL arrays contain fewer crystals.

The forward hadron (HF) calorimeter uses steel as an absorber and quartz fibers as the sensitive material. The two halves of the HF are located at 11.2 m from the interaction region, one at each end. Together they provide coverage in the range $3.0 < |\eta| < 5.2$. Each HF calorimeter consists of 432 readout towers, containing long and short quartz fibers running parallel to the beam. The long fibers run the entire depth of the HF calorimeter (165 cm, or approximately 10 interaction lengths), whereas the short fibers start at a depth of 22 cm from the front of the detector. By reading out the two sets of fibers separately, it is possible to distinguish showers generated by electrons or photons, which deposit a large fraction of their energy in the long-fiber calorimeter segment, from those generated by hadrons, which typically produce, on average, nearly equal signals in both calorimeter segments.

The triggers used in this analysis are based on signals from the Beam Pick-up and Timing for eXperiments (BPTX) detectors [31]. The BPTX devices have a time resolution of less than 0.2 ns. They are located around the beam pipe at a distance of $\pm 175$ m from the nominal interaction point, and are designed to provide precise information on the bunch structure and timing of the proton beams.

A more detailed description of the CMS detector, together with a definition of the coordinate system used and the relevant kinematic variables, can be found in Ref. [32].

### 3 Monte Carlo simulations

Two kinds of Monte Carlo (MC) event generators are used in this analysis: inclusive and exclusive generators. The inclusive generators model the inclusive diffractive dissociation [33] and nondiffractive interactions, and are used to estimate the tracking efficiency, multiple reconstruction and misreconstruction rates. The exclusive generators are used to generate CEP events and to calculate the vertex correction factors. There are no available MC event generators that produce exclusive scalar and tensor resonances via DPE, such as the production of $f_0(500)$, $f_0(980)$, and $f_2(1270)$ mesons.

Event samples are generated with various tunes for diffractive (CD) dissociation, as well as nondiffractive (ND) production [33]. The SD, DD, and ND events are generated with the CUETP8M1 tune. The Minimum Bias Rockefeller (MBR) model of PYTHIA is based on the renormalized pomeron flux model and it is capable of generating SD, DD, ND and CD events.

- **EPOS** [37] with its LHC tune [38]: This inclusive generator is based on the Regge–Gribov phenomenology [39], and it models SD, DD, CD, and ND processes.
- **STARLIGHT** [40]: This event generator models photon-photon and photon-pomeron interactions in pp and heavy ion collisions. The production of $\rho^0$ mesons and their successive decay into two pions through the VMP process is simulated by STARLIGHT. For background studies, $\omega$ mesons are also generated with STARLIGHT and their decay simulated by PYTHIA to the $\pi^+\pi^-\pi^0$ final state.
- **DIME MC 1.06** [5]: The DIME MC software describes continuum $\pi^+\pi^-$ production through DPE. The generator uses a phenomenological model based on Regge theory.

Events are generated with the Orear-type off-shell meson form factors with parameters $a_\omega = 0.71$ GeV$^{-1}$ and $b_\omega = 0.91$ GeV$^{-1}$ [5]. Furthermore, two additional MC samples are generated with an exponential form factor with $b_{\text{exp}} = 0.45$ [5] and 1 GeV$^{-2}$ [1] to study the systematic uncertainty in the measured resonance cross sections arising from uncertainties in the DIME MC parametrization.

All of the generated events are processed by a detailed GEANT4 simulation [41] of the CMS detector.

### 4 Event selection

The following triggers were employed:

- **Zero bias**: zero-bias events are selected by using either the BPTX detectors (13 TeV data) or the LHC clock signal and the known LHC bunch structure (5.02 TeV data). Both methods provided zero-bias events.
- **BPTX XOR**: Here XOR stands for the exclusive OR logic, where only one BPTX is fired, corresponding to an incoming proton bunch from only one direction. This trigger was used in both 5.02 and 13 TeV data sets.
- **No-BPTX**: There is no signal in the BPTX detectors, which means there are no incoming proton bunches. This trigger was used in both 5.02 and 13 TeV data sets.

The present analysis uses events acquired with the zero bias trigger. The BPTX XOR and No-BPTX triggers select events with no interacting bunches, which are used to estimate the electronic noise of calorimeters and possible col-
lisions between beam particles and residual gas molecules in the CMS beampipe (beam-gas background). The contribution from beam-gas collisions is negligible because there is no difference in the measured calorimeter tower energy distributions for the BPTX XOR and No-BPTX triggered events.

In the offline selections, it is required that the event has exactly two tracks, both of which satisfy \( \chi^2 / \text{ndf} < 2 \) (where the \( \chi^2 \) value is calculated based on the fitted trajectory and the measured tracker hits, and \( \text{ndf} \) is the number of degrees of freedom), \( p_T > 0.2 \text{ GeV} \), and \( |\eta| < 2.4 \) to ensure high track reconstruction efficiency. Only events with oppositely charged (opposite-sign, OS) tracks are selected for analysis. Only events with same-sign (SS) tracks are used in the background estimation.

Events with a single collision are selected by requiring the two tracks form a single reconstructed vertex subject to the constraint that

\[
|z_1 - z_2| < 3\sqrt{\sigma_1^2 + \sigma_2^2},
\]

where \( z_1 \) and \( z_2 \) are the \( z \) coordinates of the closest approach of the reconstructed tracks to the beamline, and \( \sigma_1 \) and \( \sigma_2 \) are their corresponding uncertainties.

To select exclusive events, all calorimeter towers not matching the trajectories of the two tracks must have energy deposits below a threshold, which is defined in Table 1. A tower is matched to a track if the intersection of the extrapolated trajectory with the calorimeter surface is within three standard deviations in \( \eta \) and \( \phi \) from the center of the tower. The threshold values are chosen to have a maximum 1% rejection of signal events resulting from the electronic noise of the calorimeters. Non-exclusive events might be also selected because of the lack of coverage in the eta gap between the HF and central calorimeters; these events are also taken into account in the background estimation presented later in this paper.

Using all of the above listed event selection criteria, a total of 48961 events were selected from the 5.02 TeV and 20980 from the 13 TeV dataset.

### Table 1 The value of calorimeter thresholds for different calorimeter constituents, used in the selection of exclusive events

| Calorimeter   | Threshold [GeV] | \( \eta \) coverage |
|---------------|----------------|---------------------|
| ECAL barrel   | 0.6            | \( |\eta| < 1.5 \)     |
| ECAL endcap   | 3.3            | \( 1.5 < |\eta| < 3.0 \) |
| HCAL barrel   | 2.0            | \( |\eta| < 1.3 \)     |
| HCAL endcap   | 3.8            | \( 1.3 < |\eta| < 3.0 \) |
| HF            | 4.0            | \( 3.15 < |\eta| < 5.2 \) |

### 5 Data analysis

#### 5.1 Particle identification

Particle identification is used to select pion pairs by the mean energy loss \( \langle dE/dx \rangle \) of particles in the silicon tracking detectors. The \( dE/dx \) values shown in the left panel of Fig. 2 are calculated by a second-order harmonic mean using only the strip detectors [42]:

\[
\langle dE/dx \rangle = \left( \frac{1}{N} \sum_{i=1}^{N} (\Delta E/\Delta x)^{-2} \right)^{-\frac{1}{2}},
\]

where \( N \) is the number of energy loss measurements, \( \Delta E/\Delta x \) is a single energy loss measurement per path length in one tracker module, and the sum runs over the strip detectors carrying energy loss measurements. The \(-2\) exponent in this formula suppresses high \( \Delta E/\Delta x \) values arising from the highly asymmetric \( \Delta E/\Delta x \) Landau distribution, thus avoiding a bias in the estimate of the average \( dE/dx \) of the track.

The track classification is achieved by fitting the mean energy loss distributions of tracks from low multiplicity \( (N_{\text{track}} \leq 4) \) events with a sum of three Gaussian functions corresponding to pions, kaons, and protons. An example for such a fit is shown in the right panel of Fig. 2. In the 0.3–2 GeV momentum range pions are selected from the \( \pm 3 \) standard deviation region of the corresponding Gaussian peak. This region is shown in the left panel of Fig. 2. Tracks that have \( p < 0.3 \) or \( p > 2 \text{ GeV} \) are assumed to be pions. The contamination from kaons and protons is estimated using the data-driven approach described in Sect. 5.3.

#### 5.2 Corrections

Each event is weighted by several correction factors to compensate for the detector and reconstruction effects. The multiplying factor is the product of four independent corrections: tracking, multiple reconstruction, vertex, and pileup correction.

A tracking correction is used to correct for track reconstruction inefficiencies:

\[
C_{\text{tr}} = \frac{1}{\epsilon_{\text{tr},1}} \frac{1}{\epsilon_{\text{tr},2}},
\]

where \( \epsilon_{\text{tr},1} (\epsilon_{\text{tr},2}) \) is the tracking efficiency in the region where the first (second) particle is reconstructed. A single charged particle may lead to two reconstructed tracks, such as spiralling tracks near \( \eta \approx 0 \) or split tracks in the overlap region of the tracker barrel and endcap. This effect is corrected using
Fig. 2 Left: The distribution of the logarithm of the mean energy loss and absolute value of the momentum of tracks from low-multiplicity ($N_{\text{track}} \leq 4$) events collected at $\sqrt{s} = 13$ TeV. The $\pi$-selection region is shown in the 0.3–2 GeV range. All tracks outside this momentum range are identified as pions. Right: The fit of energy loss distributions in a given momentum bin with the sum of three Gaussian curves. Plots are similar for the 5.02 TeV data.

$\varepsilon_{\text{mrec}}$, which is the probability for this situation to occur. In this case the correction factor takes the form

$$C_{\text{mrec}} = \frac{1}{1 - \varepsilon_{\text{mrec},1}} \frac{1}{1 - \varepsilon_{\text{mrec},2}}.$$  (5)

The values of $\varepsilon_{\text{tr}}$ and $\varepsilon_{\text{mrec}}$ are estimated as a function of $\eta$ and $p_T$ using MC simulations. Their dependence on the track $\phi$ and the vertex position $z$-coordinate is integrated over. The simulated events are weighted such that the vertex $z$-coordinate distribution agrees with collision data.

The vertex correction $C_{\text{vert}}$ accounts for events with an unreconstructed vertex. It is the reciprocal of the vertex efficiency, which is calculated using samples produced by the DIME MC and STARLIGHT generators. The vertex efficiency has a slight dependence on the invariant mass of the track pair that is included when applying the vertex correction.

Some real CEP events are rejected because of pileup. To account for these lost events, a correction factor $C_{\text{pu}}$ for the number of selected events can be computed. The CEP events are selected from bunch crossings with a single collision, so by assuming that the number of collisions follows a Poisson distribution, one can derive $C_{\text{pu}}$:

$$C_{\text{pu}} = \frac{N\mu}{N \mu \exp(-\mu)} = \exp(\mu).$$  (6)

Table 2 Correction factors

| Type               | Range     |
|--------------------|-----------|
| Tracking           | 1.05–1.50 |
| Multiple reconstruction | 1.005–1.040 |
| Vertex             | 1.05–1.33 |
| Pileup             | 1.3–2.1  |

Here, $\mu$ is the average number of visible inelastic collisions, in a given bunch crossing, $N$ is the total number of analyzed events. The value of $\mu$ depends on the instantaneous luminosity associated with individual bunch crossings, $L_{\text{bunch}}$, according to the following expression:

$$\mu = \frac{\sigma_{\text{inel,vis}} L_{\text{bunch}}}{f},$$  (7)

where $\sigma_{\text{inel,vis}}$ is the visible inelastic pp cross section, $f$ is the revolution frequency of protons, and $L_{\text{bunch}}$ is the average instantaneous luminosity at the given bunch crossing position for time periods of 23.3 s. The ratio of $\sigma_{\text{inel,vis}}$ to $f$ is obtained by fitting the fraction of events with no observed collisions as a function of $L_{\text{bunch}}$ with the functional form $A \exp(-b L_{\text{bunch}})$, where $A$ and $b$ are free parameters of the fit.

The range of correction factors is summarized in Table 2.
5.3 Background estimation

The main background contributions to $\pi^+\pi^-$ CEP are the multiparticle background and the exclusive $K^+K^-/\pi^0p\bar{p}$ production. The multiparticle background in the selected exclusive sample consists of events with more than two particles created in the interaction, of which only two are observed because the additional particles yield energy deposits below the thresholds, or outside the acceptance. The SD, DD, ND, and CD processes with more than two centrally produced particles belong to this contribution. A method based on control regions is used to estimate this multiparticle background. Control regions are selected in which events have at least two calorimeter towers above threshold, not matched to the two selected pions, with all the other selection criteria satisfied. The distribution of the number of events selected in this way as a function of the number of extra towers with energy above threshold is shown in Fig. 3. The counts in the bins with 2, 3, 4, and 5 towers are used to estimate the background. The normalization factor is calculated using the following assumption:

$$\frac{N_{\text{mpart,SS}}(0 \text{ extra towers})}{N_{\text{mpart,SS}}(2-5 \text{ extra towers})} = \frac{N_{\text{mpart,OS}}(0 \text{ extra towers})}{N_{\text{mpart,OS}}(2-5 \text{ extra towers})},$$

where $N_{\text{mpart,OS/SS}}$ is the number of multiparticle events with two OS or SS tracks. The validity of this assumption is checked by comparing the true and predicted number of background events in inclusive MC samples (Table 3). The observed discrepancy reflects the differences between OS and SS events and is included as a systematic uncertainty in the estimate of the total number of multiparticle background events, as discussed in Sect. 5.4. With this formula and the fact that all SS events are multiparticle events because of charge conservation, it is possible to calculate the value of $N_{\text{nhad,OS}}(0 \text{ towers})$, which is the number of multiparticle background events. The expected distribution of the multiparticle background is obtained using OS events with 2–5 extra calorimeter towers.

This method does not take into account the background contribution from $\omega \rightarrow \pi^+\pi^-\pi^0$, because this decay cannot be observed in the SS events. This latter contribution is negligible (0.5%) based on MC simulation results.

### Table 3 Checking the validity of Eq. (8) by comparing the true and predicted number of background events in inclusive MC samples

| Event generator | Difference in normalization |
|-----------------|-----------------------------|
| EPOS            | (+11 ± 4)%                  |
| PYTHIA 8 CUETP8M1 | (−5.5 ± 3)%                |
| PYTHIA 8 MBR    | (+10 ± 4)%                  |

Fig. 3 The number of extra calorimeter towers over threshold in events containing an identified pion pair with opposite (left) and same (right) charge. The known contributions, denoted with the red hatched areas, are used to estimate the background in the zero bin of the opposite-sign distribution, which is denoted by the blue hatched area. The error bars correspond to statistical uncertainties, whereas the error rectangle on the background denotes the 14% systematic uncertainty in the background normalization. Plots are similar for 5.02 TeV data.
Genuine exclusive $K^+K^-$ and $p\bar{p}$ events, where both particles are misidentified as pions, are included in the previous multiparticle background estimate. To correct for this contribution, the $K/\pi$ ratios are calculated in the exclusive events using tracks with $p < 1$ GeV. Similarly, the $p/\pi$ ratio is calculated in the same sample in the range $1 < p < 2$ GeV. The $K/\pi$ and $p/\pi$ ratios are assumed to be $0.3^{+0.1}_{-0.05}$ in the region $p > 1$ and $p > 2$ GeV, respectively [43]. Using this assumption and the measured ratios, the average $K/\pi$ and $p/\pi$ ratios are then calculated over the entire momentum range of the exclusive sample. These average ratios can then be used to compute the number of $K^+K^-$ and $p\bar{p}$ events under two extreme scenarios. The first scenario assumes that the production of a $K$ or a $p$ is always accompanied by the production of its antiparticle, whereas in the second scenario it is assumed that the production of an individual $K^+$, $K^-$, $p$, $p$,
or \( \bar{p} \) is a totally independent process. The final estimate of the exclusive \( K^+K^- \) and \( p\bar{p} \) background normalization is calculated as the average of the estimates obtained from assuming these two scenarios. According to these calculations, there is an 11% residual contribution of exclusive \( K^+K^- \) and \( p\bar{p} \) events in the sample after the multiparticle background subtraction. The background distributions of this contribution are calculated by using two-track OS exclusive events with at least one identified \( K^- \) (Fig. 4).

The estimated multiparticle and exclusive \( K^+K^-/p\bar{p} \) background distributions, as functions of the main kinematic variables, are shown in Fig. 4. These two background contributions are subtracted from the measured distributions. The background subtracted spectra are divided by the integrated luminosity to obtain the differential cross sections.

5.4 Systematic uncertainties

Systematic uncertainties in the measured cross sections originate from various sources. These include reconstruction effects, particle identification, correction factors, background estimation, and the luminosity estimation. The uncertainty assigned to the tracking efficiency in the case of a single track is 3.9% [29], which corresponds to 7.8% uncertainty for two tracks. Furthermore, the uncertainty in the multiple reconstruction rate for a single track is also 3.9%, which propagates to a maximum of 0.4% uncertainty in the cross section for two tracks, which is neglected in the analysis. Misreconstructed tracks bias the sample in two ways: either a CEP event is rejected if a third misreconstructed track is found, or an event is identified as CEP with a misreconstructed and a genuine track. This source of systematic uncertainty is estimated to be 1% for a single track, which is the maximal misreconstruction rate calculated using inclusive MC samples in the kinematic region \( \langle PT(\pi) \rangle > 0.2 \text{ GeV} \) and \( |\eta(\pi)| < 2.4 \) of the analysis. Since the probability to have two or more misreconstructed tracks in these low-multiplicity events is negligible, the final uncertainty remains 1%. From the comparison of the DIME MC and STARLIGHT simulations, the uncertainty of the vertex correction is estimated to be 1%.

The systematic uncertainty in the pileup correction factor for a single event is calculated from only the systematic uncertainties in the luminosity measurement that do not affect its overall normalization. Indeed, the normalization-related systematic uncertainties are compensated in the exponential fit described in Sect. 5.2. The uncertainties that do not affect the normalization are estimated to be 1.6% and 1.5% for 5.02 [44] and 13 TeV [45] data, respectively. These values propagate to a 1% uncertainty in the pileup correction factor for a single event. After adding up all the selected events, the pileup uncertainty becomes smaller than 0.1%, which is neglected in the following.

The measured signal yield is affected by the uncertainty arising from the two effects associated with calorimeter noise and veto inefficiency caused by the adopted energy thresholds. A genuine CEP event can be erroneously discarded if the calorimeter noise appears above the energy thresholds used in the veto. Conversely, a nonCEP event can pass the final selection if the extra particles pass the veto requirements. In the HF, these uncertainties are estimated by varying the calorimeter energy thresholds by \( \pm 10% \) [46]. The resulting uncertainty is estimated to be 3% for both the 5.02 and 13 TeV data sets. Similarly, the ECAL and HCAL thresholds are varied by \( \pm 5% \) [47,48], which results in a 1% uncertainty in the corrected yields at both energies.

The systematic uncertainty estimation of the multiparticle background is done by varying the control region used in the background estimation procedure: 1–2, 2–9, and 5–9 extra towers. The estimate of the systematic uncertainty in the multiparticle background normalization is 10%. Additionally, a 10% uncertainty is added to this value quadratically, taking into account the deviations shown in Table 3; thus the final uncertainty in the multiparticle background normalization is 14%. After subtracting this contribution, this propagates to systematic uncertainties depending on the invariant mass, transverse momentum and rapidity of the pion pair. The multiparticle background estimation uncertainty varies between 10–20% below 1500 MeV. Over 1500 MeV the uncertainty varies between 20–60%, because the signal versus background ratio is much smaller. The average uncertainty, used as the systematic uncertainty of the total cross section, is 15%.

The exclusive \( K^+K^- \) and \( p\bar{p} \) background uncertainty comes from three sources: (1) multiparticle contamination in the \( dE/dx \) vs. momentum distribution that modifies the \( K/\pi \) and \( p/\pi \) ratios, (2) the uncertainty in the \( K/\pi \) ratio above 1 GeV, and (3) the uncertainty in the \( p/\pi \) ratio above 2 GeV. The multiparticle contamination is estimated by checking the difference between two extreme cases: all particle types are produced independently, or the sample is purely exclusive. The results correspond to an uncertainty of 70% in the normalization of this background contribution at both energies. To account for the uncertainty of \( K/\pi \) above 1 GeV and \( p/\pi \) over 2 GeV, the exclusive background normalization is calculated assuming different values (0.25, 0.30, and 0.40 [43]) for the \( K/\pi \) and \( p/\pi \) ratios in these regions. The uncertainties assigned to these effects are 16 and 4%, respectively. Thus the total systematic uncertainty of the exclusive \( K^+K^- \) and \( p\bar{p} \) background normalization is 72%. After subtracting this background contribution, this propagates to systematic uncertainties, which depend on the invariant mass, transverse momentum, and rapidity of the pion pair. The typical range of this systematic uncertainty contribution is 5–20%. For the total cross section, this source contributes to an average uncertainty of 6%.
Table 4  The sources and average values of systematic uncertainties, used as the systematic uncertainty of the total cross section

| Source                                               | Average value |
|------------------------------------------------------|---------------|
| Tracking efficiency                                  | 7.8%          |
| Misreconstructed tracks                              | 1%            |
| Vertex                                               | 1%            |
| HF energy scale                                      | 3%            |
| ECAL and HCAL energy scale                           | 1%            |
| Multiparticle background                             | 15%           |
| Exclusive K+K− and pP̅ background                     | 6%            |
| Total w/o int. luminosity                            | 18.3%         |
| + Integrated luminosity                              | 2.3%          |

All of the systematic uncertainties listed above are the same for the 5.02 and 13 TeV data sets. Additionally, the systematic uncertainty in the integrated luminosity is 2.3\% [44,45]. The average values of the systematic uncertainties are summarized in Table 4. The total systematic uncertainty is obtained by adding the individual contributions in quadrature. All systematic uncertainty contributions are considered fully correlated across invariant mass bins.

6 Results

The differential cross sections are calculated from the selected events as functions of the invariant mass, transverse momentum, and rapidity of the pion pair. These are shown in Fig. 5 with the generator-level predictions from the STARLIGHT and DIME MC generators, normalized to their cross sections. The MC generators provide an incomplete description of the available data, since they do not model the 4\pi production spectrum as these MC event generators do not model the forward dissociation of protons.

The total cross section of the CEP process with two pions in the final state in the kinematic region $p_T(\pi) > 0.2$ GeV and $|\eta(\pi)| < 2.4$ is obtained by integrating the observed spectra in this region:

$$\sigma_{pp \rightarrow p\pi^+\pi^-} (\sqrt{s} = 5.02$ TeV) $= 32.6 \pm 0.7$ (stat) $\pm 6.0$ (syst) $\pm 0.8$ (lumi) \, \mu b,$$  \hspace{1cm} (9)

$$\sigma_{pp \rightarrow p\pi^+\pi^-} (\sqrt{s} = 13$ TeV) $= 33.7 \pm 1.0$ (stat) $\pm 6.2$ (syst) $\pm 0.8$ (lumi) \, \mu b.$$  \hspace{1cm} (10)

Below, it is demonstrated that the measured invariant $\pi^+\pi^-$ mass spectrum is well-described by the sum of the continuum distribution obtained from the DIME MC model and four dominant resonances, modeled here by Breit-Wigner functions. In the fitting procedure the quantum mechanical interference effect and the detector resolution are also included.

The following fit function is used:

$$f(m) = \int G(m - m' ; \sigma) \left[ |A_{RBW}^{\rho}(m')|^2 + |A_{RBW}^{f0(500)}(m')|^2 e^{i\phi_{f0(500)}(m')} + |A_{RBW}^{f0(980)}(m')|^2 e^{i\phi_{f0(980)}(m')} + |A{}_{RBW}^{f2}(m')|^2 e^{i\phi_f(m')} + b B_{DIME}(m') \right]^2 dm'.$$  \hspace{1cm} (11)

Here $G(m; \sigma)$ is a Gaussian distribution with variance $\sigma$ and zero mean, $B_{DIME}(m)$ is the nonresonant background estimated from the DIME MC using the Orear-type form factor, and $b$ is a scale factor for the continuum contribution, and $\phi_{f0(500)}$, $\phi_{f0(980)}$, and $\phi_f$ are phases that characterize interference effects. The $A_{RBW}^{\rho}(m)$ is the relativistic Breit–Wigner amplitude, which can be written as [49]:

$$A_{RBW}^{\rho}(m) = A_{\rho} \frac{\sqrt{m M_{\rho} \Gamma(m)} \left( m - M_{\rho} + i M_{\rho} \Gamma(m) \right)}{m^2 - M_{\rho}^2 + i M_{\rho} \Gamma(m)},$$  \hspace{1cm} (12)

$$\Gamma(m) = \Gamma_i \frac{M_i}{m} \left[ \frac{m^2 - 4 m^2_{\rho} M_i^2}{M_i^2 - 4 m^2_{\rho}} \right]^{1/2}.$$.  \hspace{1cm} (13)

where $A_{\rho}$, $M_i$, and $\Gamma_i$ are the yield, mass, and width of the resonance, respectively, $m_{\rho}$ is the mass of charged pions, and $J$ is the total angular momentum of the resonance. According to Ref. [2], the magnitude of the interference between the DPE and VMP processes is around 1\%, therefore no interference term is used between $\rho^0$ and DPE resonances. The convolution with the Gaussian distribution models the mass resolution of the detector.

The mass resolution ($\sigma$) is calculated by fitting the distribution of the difference between generator-level and reconstructed mass from the STARLIGHT and DIME MC simulations. Based on these calculations, the mass resolution is found to vary from 9 to 14 MeV in the mass range 500–2000 MeV. In the final fit, an effective mass resolution of 11 MeV is used and the systematic uncertainty associated with this value is
Fig. 5 Differential cross sections as functions of mass (upper row), transverse momentum (middle row), and rapidity (bottom row), compared with generator-level simulations for the 5.02 (left) and 13 TeV (right) data sets. The error bars correspond to statistical, whereas the open boxes to systematic uncertainties.
Cross sections of the resonant processes in the $p_T(\pi) > 0.2$ GeV, $|\eta(\pi)| < 2.4$ fiducial region, extracted from the simple model fit using the sum of the continuum distribution obtained from the DIME MC model and four dominant resonances. The luminosity-related uncertainties are included in the systematic uncertainties. The STARLIGHT predictions for $pp \to p'p\rho^0 \to p'p\pi^+\pi^-$ processes are 2.3 and 3.0 $\mu$b for 5.02 and 13 TeV, respectively, which is compatible with the fit results for the 5.02 (left) and 13 TeV (right) data sets. The error bars correspond to statistical, whereas the open boxes correspond to systematic uncertainties [24] and the resulting variation in the cross section of the resonances is added in quadrature to the other systematic uncertainty contributions. Furthermore the fit is repeated with the two other DIME MC settings and the variation in the cross section is taken as an additional systematic uncertainty and added in quadrature to the other uncertainties.

The above simple model fit also provides values for the cross sections of the resonances; these are obtained by integrating the fitted squared amplitudes from the dipion threshold $(2m_\pi)$ to $M_i + 5\Gamma_i$:

$$
\sigma_{i,\text{res}} = \int_{2m_\pi}^{M_i + 5\Gamma_i} |A_{RBW,i}(m)| dm. \tag{14}
$$

The fits are shown in Fig. 6 and the cross sections are summarized in Table 5.

The model of interfering Breit–Wigner resonances with a continuum gives a good description of the data in the region of resonant peaks (below 1500 MeV). The cross sections for $\rho^0(770)$ production calculated from the fits are slightly larger than the predicted values from STARLIGHT, which are 2.3 and 3.0 $\mu$b for 5.02 and 13 TeV, respectively. The differences can be attributed to the additional semieclusive contribution that is not modeled by STARLIGHT. The values of the scale parameter $b$ are 0.7 ± 0.2 for 5.02 TeV and 1.1 ± 0.3 for 13 TeV, and therefore they are consistent within uncertainties for the two energies.
7 Summary

The cross sections for central exclusive pion pair production have been measured in pp collisions at 5.02 and 13 TeV center-of-mass energies. Exclusive events are selected by vetoing additional energy deposits in the calorimeters and by requiring two oppositely charged pions identified via their mean energy loss in the tracker detectors. These events are used together with correction factors to obtain invariant mass, transverse momentum, and rapidity distributions of the $\pi^+\pi^-$ system. The measured total exclusive $\pi^+\pi^-$ production cross section is 32.6 $\pm$ 0.7 (stat) $\pm$ 6.0 (syst) $\pm$ 0.8 (lumi) and 33.7 $\pm$ 1.0 (stat) $\pm$ 6.2 (syst) $\pm$ 0.8 (lumi) $\mu$b for 5.02 and 13 TeV, respectively. The observed mass spectrum exhibits resonant structures, which can be fitted with a simple model containing four interfering Breit-Wigner functions, corresponding to the $f_0(500)$, $\rho^0(770)$, $f_2(980)$, and $f_2(1270)$ resonances, and a continuum contribution modeled by the DIME MC. The exclusive production cross sections are extracted from this fit. The obtained cross sections of $\rho^0(770)$ production are higher than the STARLIGHT model prediction, which can be explained by the presence of semiexclusive production which is not modeled by the STARLIGHT generator.

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CMS Collaboration

Yerevan Physics Institute, Yerevan, Armenia
A. M. Sirunyan 1, A. Tumasyan

Institut für Hochenergiephysik, Wien, Austria
W. Adam, F. Ambrogi, T. Bergauer, J. Brandstetter, M. Dragicevic, J. Erö, A. Escalante Del Valle, M. Flechtl, R. Frühwirth 1, M. Jeitler 1, N. Krammer, I. Krätschmer, D. Liko, T. Madlener, I. Mikulec, N. Rad, J. Schieck 1, R. Schönbeck, M. Spanring, D. Spitzbart, W. Waltenberger, J. Wittmann, C.-E. Wulz 1, M. Zarucki

Institute for Nuclear Problems, Minsk, Belarus
V. Drugakov, V. Moshoslov, J. Suarez Gonzalez

Universiteit Antwerpen, Antwerpen, Belgium
M. R. Darwish, E. A. De Wolf, D. Di Croce, X. Janssen, J. Lauwers, A. Lelek, M. Pieters, H. Rejeb Sfar, H. Van Haevermaet, P. Van Mechelen, S. Van Putte, N. Van Remortel

Vrije Universiteit Brussel, Brussel, Belgium
F. Blekman, E. S. Bols, S. S. Chhibra, J. D’Hondt, J. De Clercq, D. Lontkovskyi, S. Lovette, I. Marchesini, S. Moortgat, L. Moreels, Q. Python, K. Skovpen, S. Tavernier, W. Van Doninck, P. Van Mulders, I. Van Parijs

Université Libre de Bruxelles, Bruxelles, Belgium
D. Beghin, B. Bilin, H. Brun, B. Clerbaux, G. De Lentdecker, H. Delannoy, B. Dorney, L. Favart, A. Grebenyuk, A. Kalsi, L. Luetic, A. Popov, N. Postiau, E. Starling, L. Thomas, C. Vander Velde, P. Vanlaer, D. Vannerom, Q. Wang

Ghent University, Ghent, Belgium
T. Cornelis, D. Dobur, I. Khvastunov 1, C. Roskas, D. Trocino, M. Tytgat, W. Verbeke, B. Vermassen, M. Vit, N. Zaganidis

Université Catholique de Louvain, Louvain-la-Neuve, Belgium
O. Bondu, G. Bruno, C. Caputo, P. David, C. Delaere, M. Delcourt, A. Giammanco, G. Krintiras, V. Lemaitre, A. Magitteri, K. Piotrzkowski, J. Prisciandaro, A. Saggio, M. Vidal Marono, P. Vischia, J. Zobec

Centro Brasileiro de Pesquisas Fisicas, Rio de Janeiro, Brazil
F. L. Alves, G. A. Alves, G. Correia Silva, C. Hensel, A. Moraes, P. Rebello Teles

Universidade do Estado do Rio de Janeiro, Rio de Janeiro, Brazil
E. Belchior Batista Das Chagas, W. Carvalho, J. Chinellato 1, E. Coelho, E. M. Da Costa, G. G. Da Silveira 1,
Universidade Estadual Paulista\textsuperscript{a}, Universidade Federal do ABC\textsuperscript{b}, São Paulo, Brazil
S. Ahuja\textsuperscript{a}, C. A. Bernardes\textsuperscript{a}, L. Calligaris\textsuperscript{a}, T. R. Fernandez Perez Tomei\textsuperscript{a}, E. M. Gregores\textsuperscript{b}, D. S. Lemos, P. G. Mercadante\textsuperscript{b}, S. F. Novaes\textsuperscript{a}, Sandra S. Padula\textsuperscript{a}

Institute for Nuclear Research and Nuclear Energy, Bulgarian Academy of Sciences, Sofia, Bulgaria
A. Aleksandrov, G. Antchev, R. Hadjiiska, P. Iaydjiev, A. Marinov, M. Misheva, M. Rodozov, M. Shopova, G. Sultanov

University of Sofia, Sofia, Bulgaria
A. Dimitrov, L. Litov, B. Pavlov, P. Petkov

Beihang University, Beijing, China
W. Fang\textsuperscript{9}, X. Gao\textsuperscript{7}, L. Yuan

Department of Physics, Tsinghua University, Beijing, China
Z. Hu, Y. Wang

Institute of High Energy Physics, Beijing, China
M. Ahmad, G. M. Chen, H. S. Chen, M. Chen, C. H. Jiang, D. Leggat, H. Liao, Z. Liu, S. M. Shaheen\textsuperscript{8}, A. Spiezia, J. Tao, E. Yazgan, H. Zhang, S. Zhang\textsuperscript{8}, J. Zhao

State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China
A. Agapitos, Y. Ban, G. Chen, A. Levin, J. Li, L. Li, Q. Li, Y. Mao, S. J. Qian, D. Wang

Universidad de Los Andes, Bogota, Colombia
C. Avila, A. Cabrera, L. F. Chaparro Sierra, C. Florez, C. F. González Hernández, M. A. Segura Delgado

Faculty of Electrical Engineering, Mechanical Engineering and Naval Architecture, University of Split, Split, Croatia
D. Giljanović, N. Godinovic, D. Lelas, I. Puljak, T. Sculac

Faculty of Science, University of Split, Split, Croatia
Z. Antunovic, M. Kovac

Institute Rudjer Boskovic, Zagreb, Croatia
V. Briljевич, S. Ceci, D. Ferencek, K. Kadija, B. Mesic, M. Roguljic, A. Starodumov\textsuperscript{9}, T. Susa

University of Cyprus, Nicosia, Cyprus
M. W. Ather, A. Attikis, E. Erodotou, A. Ioannou, M. Kolosova, S. Konstantinou, G. Mavromanolakis, J. Mousa, C. Nicolaou, P. Ptochos, P. A. Razis, H. Rykaczewski, D. Tsiakkouri

Charles University, Prague, Czech Republic
M. Finger\textsuperscript{10}, M. Finger Jr.\textsuperscript{10}, A. Kveton, J. Tomsa

Escuela Politecnica Nacional, Quito, Ecuador
E. Ayala

Universidad San Francisco de Quito, Quito, Ecuador
E. Carrera Jarrin

Academy of Scientific Research and Technology of the Arab Republic of Egypt, Egyptian Network of High Energy Physics, Cairo, Egypt
M. A. Mahmoud\textsuperscript{11,12}, Y. Mohammed\textsuperscript{11}

National Institute of Chemical Physics and Biophysics, Tallinn, Estonia
S. Bhowmik, A. Carvalho Antunes De Oliveira, R. K. Dewanjee, K. Ehataht, M. Kadastik, M. Raidal, C. Veelken

Department of Physics, University of Helsinki, Helsinki, Finland
P. Eerola, L. Forthomme, H. Kirschenmann, K. Osterberg, J. Pekkanen, M. Voutilainen
Helsinki Institute of Physics, Helsinki, Finland
F. Garcia, J. Havukainen, J. K. Heikkilä, T. Järvinen, V. Karimäki, R. Kinnunen, T. Lampén, K. Lassila-Perini, S. Laurila, S. Lehti, T. Lindén, P. Luukka, T. Mäenpää, H. Siikonen, E. Tuominen, J. Tuominiemi

Lappeenranta University of Technology, Lappeenranta, Finland
T. Tuuva

IRFU, CEA, Université Paris-Saclay, Gif-sur-Yvette, France
M. Besançon, F. Coudere, M. Dejardin, D. Denegri, B. Fabbro, J. L. Faure, F. Ferri, S. Ganjou, A. Givernaud, P. Gras, G. Hamel de Monchenault, P. Jarry, C. Leloup, E. Locci, J. Malecs, J. Rander, A. Rosowsky, M. Ō. Sahin, A. Savoy-Navarro 13, M. Titov

Laboratoire Leprince-Ringuet, CNRS/IN2P3, Ecole Polytechnique, Institut Polytechnique de Paris, Paris, France
C. Amendola, F. Beaudette, P. Busson, C. Charlot, B. Diab, R. Granier de Cassagnac, I. Kucher, A. Lobanov, C. Martin Perez, M. Nguyen, C. Ochando, P. Paganini, J. Rembser, R. Salerno, J. B. Sauvan, Y. Siroy, A. Zabi, A. Zghiche

Université de Strasbourg, CNRS, IPHC UMR 7178, Strasbourg, France
J.-L. Agram 14, J. Andrea, D. Bloch, G. Bourgatte, J.-M. Brom, E. C. Chabert, C. Collard, E. Conte 14, J.-C. Fontaine 14, D. Gelé, U. Goerlach, M. Jansová, A.-C. Le Bihan, N. Tonon, P. Van Hove

Centre de Calcul de l’Institut National de Physique Nucléaire et de Physique des Particules, CNRS/IN2P3, Villeurbanne, France
S. Gadrat

Université Lyon, Université Claude Bernard Lyon 1, CNRS-IN2P3, Institut de Physique Nucléaire de Lyon, Villeurbanne, France
S. Beauceron, C. Bernet, G. Boudoul, C. Camen, N. Chanon, R. Chierici, D. Contardo, P. Depasse, H. El Mamouni, J. Fay, S. Gascon, M. Gouzevitch, B. Ille, Sa. Jain, F. Lagarde, I. B. Laktineh, H. Lattaud, M. Lethuillier, L. Mirabito, S. Perries, V. Sordini, G. Touquet, M. Vander Donckt, S. Viret

Georgian Technical University, Tbilisi, Georgia
T. Torishvili 15

Tbilisi State University, Tbilisi, Georgia
Z. Tsalamalidze 10

RWTH Aachen University, I. Physikalisches Institut, Aachen, Germany
C. Autermann, L. Feld, M. K. Kiesel, K. Klein, M. Lipinski, D. Meuser, A. Pauls, M. Preuten, M. P. Rauch, C. Schomakers, J. Schulz, M. Teroerde, B. Wittmer

RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany
A. Albert, M. Erdmann, S. Erdei, T. Esch, B. Fischer, R. Fischer, S. Ghosh, T. Hebbeker, K. Hoepfner, H. Keller, L. Mastrolorenzo, M. Merschmeyer, A. Meyer, P. Millet, G. Mocellin, S. Mondal, S. Mukherjee, D. Noll, A. Novak, T. Pook, A. Pozdnyakov, T. Quast, M. Radziej, Y. Rath, H. Reithler, M. Rieger, A. Schmidt, S. C. Schuler, A. Sharma, S. Thier, S. Wiedenbeck

RWTH Aachen University, III. Physikalisches Institut B, Aachen, Germany
G. Flügge, W. Haj Ahmad 16, O. Hlushchenko, T. Kress, T. Müller, A. Nehrkorn, A. Nowack, C. Pistone, O. Pooth, D. Roy, H. Sert, A. Stahl 17

Deutsches Elektronen-Synchrotron, Hamburg, Germany
M. Aldaya Martin, C. Asawatangtrakuldee, P. Asmuss, I. Babounikau, H. Bakhshiansohi, K. Beernaert, O. Behnke, U. Behrens, A. Bermúdez Martínez, D. Bertsche, A. A. Bin Anuar, K. Borras 18, V. Botta, A. Campbell, A. Cardini, P. Connor, S. Consuegra Rodríguez, C. Contreras-Campana, V. Danilov, A. De Wit, M. M. Defranchis, C. Diez Pardos, D. Domínguez Damiani, G. Eckerlin, D. Eckstein, T. Eichhorn, A. Elwood, E. Eren, E. Gallo 19, A. Geiser, J. M. Grados Luyando, A. Grohsjean, M. Guthoff, M. Haranko, A. Harb, N. Z. Jomhari, H. Jung, A. Kasem 18, M. Kasemann, J. Keaveney, C. Kleinwort, J. Knolle, D. Krücker, W. Lange, T. Lenz, J. Leonard, J. Lidrych, K. Lipka, W. Lohmann 20, R. Mankel, I.-A. Melzer-Pellmann, A. B. Meyer, M. Meyer, M. Missiroli, G. Mittag, J. Mnich, A. Mussgiller, V. Myronenko, D. Pérez Adán, S. K. Pflictsch, D. Pfitz, A. Raspereza, A. Saibel, M. Savitskyi, V. Scheurer,
Seoul National University, Seoul, Korea
J. Almond, J. H. Bhyun, J. Choi, S. Jeon, J. Kim, J. S. Kim, H. Lee, K. Lee, S. Lee, K. Nam, S. B. Oh, B. C. Radburn-Smith, S. h. Seo, U. K. Yang, H. D. Yoo, I. Yoon, G. B. Yu

University of Seoul, Seoul, Korea
D. Jeon, H. Kim, J. H. Kim, J. S. H. Lee, I. C. Park, I. Watson

Sungkyunkwan University, Suwon, Korea
Y. Choi, C. Hwang, Y. Jeong, J. Lee, Y. Lee, I. Yu

Riga Technical University, Riga, Latvia
V. Veckalns

Vilnius University, Vilnius, Lithuania
V. Dudenas, A. Juodagalvis, J. Vaitkus

National Centre for Particle Physics, Universiti Malaya, Kuala Lumpur, Malaysia
Z. A. Ibrahim, F. Mohamad Idris, W. A. T. Wan Abdullah, M. N. Yusli, Z. Zolkapli

Universidad de Sonora (UNISON), Hermosillo, Mexico
J. F. Benitez, J. A. Carrillo-Valdez, E. De La Cruz-Burelo, I. Heredia-De La Cruz, R. Lopez-Fernandez, A. Sanchez-Hernandez

Universidad Iberoamericana, Mexico City, Mexico
A. Morelos Pineda

University of Montenegro, Podgorica, Montenegro
N. Raicevic

University of Auckland, Auckland, New Zealand
D. Krofcheck

University of Canterbury, Christchurch, New Zealand
S. Bheesette, P. H. Butler

National Centre for Physics, Quaid-I-Azam University, Islamabad, Pakistan
A. Ahmad, M. Ahmad, Q. Hassan, H. R. Hoorani, W. A. Khan, M. A. Shah, M. Shoaib, M. Waqas

AGH University of Science and Technology Faculty of Computer Science, Electronics and Telecommunications, Kraków, Poland
V. Avati, L. Grzanka, M. Malawski

National Centre for Nuclear Research, Swierk, Poland
H. Białkowska, M. Błuj, B. Boinska, M. Górski, M. Kazana, M. Szleper, P. Zalewski

Institute of Experimental Physics, Faculty of Physics, University of Warsaw, Warsaw, Poland
K. Bunkowski, A. Byszuk, K. Doroba, A. Kalinowski, M. Konecki, J. Krolikowski, M. Misiura, M. Olszewski, A. Pyskir, M. Walczak

Laboratório de Instrumentação e Física Experimental de Partículas, Lisbon, Portugal
M. Araújo, P. Bargassa, D. Bastos, A. Di Francesco, P. Faccioli, B. Galinha, M. Gallinaro, J. Hollar, N. Leonardo, J. Seixas, G. Strong, O. Toldaiev, J. Varela

Joint Institute for Nuclear Research, Dubna, Russia
S. Afanasiev, P. Bunin, M. Gavrilenko, I. Golutvin, I. Gorbunov, A. Kamenev, V. Karjavin, A. Lanev, A. Malakhov, ...
Instituto de Física de Cantabria (IFCA), CSIC-Universidad de Cantabria, Santander, Spain
I. J. Cabrillo, A. Calderon, B. Chazin Quero, J. Duarte Campderros, M. Fernandez, P. J. Fernández Manteca, A. García Alonso, G. Gomez, C. Martinez Rivero, P. Martinez Ruiz del Arbol, F. Matorras, J. Piedra Gomez, C. Prieels, T. Rodrigo, A. Ruiz-Jimeno, L. Scodellaro, N. Trevisani, I. Vila, J. M. Vizan Garcia

University of Colombo, Colombo, Sri Lanka
D. U. J. Sonnadara

Department of Physics, University of Ruhuna, Matara, Sri Lanka
W. G. D. Dharmaratna, N. Wickramage

CERN, European Organization for Nuclear Research, Geneva, Switzerland
D. Abbaneo, B. Akgun, E. Auffray, G. Auzinger, J. Baechler, P. Baillon, A. H. Ball, D. Barney, J. Bendavid, M. Bianco, A. Bocci, E. Bossini, C. Bottola, E. Brondolin, T. Camporesi, A. Caratelli, G. Cerminara, E. Chapon, G. Cucciati, D. d’Enterria, A. Dabrowski, N. Daci, V. Daponte, A. David, A. De Roeck, N. Deelen, M. Deile, M. Dobson, M. Dünser, N. Dupont, A. Elliott-Peisert, F. Fallavollita, D. Fasanella, G. Franzoni, J. Fulcher, W. Funk, S. Giani, D. Giga, A. Gilbert, K. Gill, F. Glege, M. Gruchala, M. Gülbaud, D. Gulhan, J. Hegeman, C. Heidegger, Y. Iiyama, V. Innocente, A. Jafari, P. Janot, O. Karacheban, J. Kaspur, J. Kieseler, M. Krammer, C. Lange, P. Lecoq, C. Lourenço, L. Malgeri, M. Mannelli, A. Massironi, F. Meijsers, J. A. Merlin, S. Mersi, E. Meschi, F. Moortgat, M. Mulders, J. Nghiuba, S. Nourbakhsh, S. Orfanelli, L. Orsini, F. Pantaleo, L. Pape, E. Perez, M. Peruzzi, A. Petrilli, G. Petrucciani, A. Pfeiffer, M. Pierini, F. M. Pitters, M. Quinto, D. Rabady, A. Racz, M. Rovere, H. Sakulin, C. Schäfer, C. Schwick, M. Selvaggi, A. Sharma, P. Silva, W. Snoeys, P. Spichas, J. Steggemann, V. R. Tavolaro, D. Treille, A. Tsiour, A. Vartak, M. Verzetti, W. D. Zeuner

Paul Scherrer Institut, Villigen, Switzerland
L. Caminada, K. Deeters, W. Erdmann, R. Horisberger, Q. Ingram, H. C. Kaestli, D. Kotlinski, U. Langenegger, R. Wallny, D. H. Zhu

ETH Zurich-Institute for Particle Physics and Astrophysics (IPA), Zurich, Switzerland
M. Backhaus, P. Berger, N. Chernyavskaya, G. Dissertori, M. Dittmar, M. Donegà, C. Dorfer, T. A. Gómez Espinosa, C. Grab, D. Hits, T. Klijnsma, W. Lustermann, R. A. Manzoni, M. Marionneau, M. T. Meinhard, F. Micheli, M. Musella, F. Nessi-Tedaldi, F. Pauss, G. Perrin, L. Perrozzi, S. Pigazzini, M. Reichmann, C. Reissel, T. Reitenspiess, D. Ruini, D. A. Sanz Becerra, M. Schönberger, L. Shchutska, M. L. Vesterbacka Olsson, R. Wallny, D. H. Zhu

Universität Zürich, Zurich, Switzerland
T. K. Aarrestad, C. Amsler, D. Brzhechko, M. F. Canelli, A. De Cosa, R. Del Burgo, S. Donato, C. Galloni, B. Kilminster, S. Leontsinis, V. M. Mikuni, I. Neutelings, G. Raucu, P. Robmann, D. Salerno, K. Schweiger, C. Seitz, Y. Takahashi, S. Wertz, A. Zucchetta

National Central University, Chung-Li, Taiwan
T. H. Doan, C. M. Kuo, W. Lin, S. S. Yu

National Taiwan University (NTU), Taipei, Taiwan
P. Chang, Y. Chao, K. F. Chen, P. H. Chen, W.-S. Hou, Y. y. Li, R.-S. Lu, E. Paganis, A. Psallidas, A. Steen

Department of Physics, Faculty of Science, Chulalongkorn University, Bangkok, Thailand
B. Asavapirobhoph, N. Srimanobhas, N. Suwonjandee

Physics Department, Science and Art Faculty, Çukurova University, Adana, Turkey
M. N. Bakirci, A. Bat, B. Boran, S. Damarseckin, Z. S. Demiroglu, F. Dolek, C. Dozen, I. Dumanoglu, S. Girgis, G. Gokbulut, EmineGurpinar Guler, Y. Guler, I. Ho, C. Isik, E. E. Kangal, O. Kara, A. Kayis Topaksu, U. Kiminsu, M. Oglakci, G. Onengut, K. Ozdemir, A. E. Simsek, D. Sunar Cerci, U. G. Tok, S. Turkacpar, I. S. Zorbakir, C. Zorbilmez

Physics Department, Middle East Technical University, Ankara, Turkey
B. Isildak, G. Karapinar, M. Yalvac

Bogazici University, Istanbul, Turkey
I. O. Atakisi, E. Gülmez, M. Kaya, O. Kaya, B. Kaynak, Ö. Özçelik, S. Ozkorucuklu, S. Tekten, E. A. Yetkin
Istanbul Technical University, Istanbul, Turkey
A. Cakir, K. Cankocak, Y. Komurcu, S. Sen

Institute for Scintillation Materials of National Academy of Science of Ukraine, Kharkov, Ukraine
B. Grynyov

National Scientific Center, Kharkov Institute of Physics and Technology, Kharkov, Ukraine
L. Levchuk

University of Bristol, Bristol, UK
F. Ball, E. Bhal, S. Bologna, J. J. Brooke, D. Burns, E. Clement, D. Cussans, O. Davignon, H. Flacher, J. Goldstein, G. P. Heath, H. F. Heath, L. Kreczko, S. Paramesvaran, B. Penning, T. Sakuma, S. Seif El Nasr-Storey, D. Smith, V. J. Smith, J. Taylor, A. Titterton

Rutherford Appleton Laboratory, Didcot, UK
K. W. Bell, A. Belyaev, C. Brew, R. M. Brown, D. Cieri, D. J. A. Cockerill, J. A. Coughlan, K. Harder, S. Harper, J. Linacre, K. Manolopoulos, D. M. Newbold, E. Olaiya, D. Petyt, T. Reis, T. Schuh, C. H. Shepherd-Themistocleous, A. Thea, I. R. Tomalin, T. Williams, W. J. Womersley

Imperial College, London, UK
R. Bainbridge, P. Bloch, J. Borg, S. Breeze, O. Buchmuller, A. Bundock, GurpreetSingh CHAHAL, D. Colling, P. Dauncey, G. Davies, M. Della Negra, R. Di Maria, P. Everaerts, G. Hall, G. Iles, T. James, M. Komm, C. Laner, L. Lyons, A.-M. Magnan, S. Malik, A. Martelli, V. Milosevic, J. Nash, V. Palladino, M. Pesaresi, D. M. Raymond, A. Richards, A. Rose, E. Scott, C. Seez, A. Shtipliyski, M. Stoye, T. Strebler, S. Summers, A. Tapper, K. Uchida, T. Virdee, N. Wardle, D. Winterbottom, J. Wright, A. G. Zecchinelli, S. C. Zenz

Brunel University, Uxbridge, UK
J. E. Cole, P. R. Hobson, A. Khan, P. Kyberd, C. K. Mackay, A. Morton, I. D. Reid, L. Teodorescu, S. Zahid

Baylor University, Waco, USA
K. Call, J. Dittmann, K. Hatakeyama, C. Madrid, B. McMaster, N. Pastika, C. Smith

Catholic University of America, Washington, D.C., USA
R. Bartek, A. Dominguez, R. Uniyal

The University of Alabama, Tuscaloosa, USA
A. Buccilli, S. I. Cooper, C. Henderson, P. Rumerio, C. West

Boston University, Boston, USA
D. Arcaro, T. Bose, Z. Demiragli, D. Gastler, S. Girgis, D. Pinna, C. Richardson, J. Rohlf, D. Sperka, I. Suarez, L. Sulak, D. Zou

Brown University, Providence, USA
G. Benelli, B. Burkle, X. Coubez, D. Cutts, M. Hadley, J. Hakala, U. Heintz, J. M. Hogan, K. H. M. Kwok, E. Laird, G. Landsberg, J. Lee, Z. Mao, M. Narain, S. Sagir, R. Syarif, E. Usai, D. Yu

University of California, Davis, USA
R. Band, C. Brainerd, R. Breedon, M. Calderon De La Barca Sanchez, M. Chertok, J. Conway, R. Conway, P. T. Cox, R. Erbacher, C. Flores, G. Funk, F. Jensen, W. Ko, O. Kuwano, R. Lander, M. Mulhearn, D. Pellett, J. Pilot, M. Shi, D. Stolp, D. Taylor, K. Tos, M. Tripathi, Z. Wang, F. Zhang

University of California, Los Angeles, USA
M. Bachtis, C. Bravo, R. Cousins, A. Dasgupta, A. Florent, J. Hauser, M. Ignatenko, N. McCall, S. Regnard, D. Saltzberg, C. Schnaible, V. Valuev

University of California, Riverside, Riverside, USA
K. Burt, R. Clare, J. W. Gary, S. M. A. Ghiasi Shirazi, G. Hanson, G. Karapostoli, E. Kennedy, O. R. Long, M. Olmedo Negrete, M. I. Paneva, W. Si, L. Wang, H. Wei, S. Wimpenny, B. R. Yates, Y. Zhang
Johns Hopkins University, Baltimore, USA
B. Blumenfeld, A. Cocoros, N. Eminizer, D. Fehling, L. Feng, A. V. Gritsan, W. T. Hung, P. Maksimovic, J. Roskes, M. Swartz, M. Xiao

The University of Kansas, Lawrence, USA
C. Baldenegro Barrera, P. Baringer, A. Bean, S. Boren, J. Bowen, A. Bylinkin, T. Isidori, S. Khalil, J. King, A. Kropivnitskaya, C. Lindsay, D. Majumder, W. Mcbrayer, N. Minafra, M. Murray, C. Rogan, C. Royon, S. Sanders, E. Schmitz, J. D. Tapia Takaki, Q. Wang, J. Williams

Kansas State University, Manhattan, USA
S. Duric, A. Ivanov, K. Kaadze, D. Kim, Y. Maravin, D. R. Mendis, T. Mitchell, A. Modak, A. Mohammadi

Lawrence Livermore National Laboratory, Livermore, USA
F. Rebassoo, D. Wright

University of Maryland, College Park, USA
A. Baden, O. Baron, A. Belloni, S. C. Eno, Y. Feng, N. J. Hadley, S. Jabeen, G. Y. Jeng, R. G. Kellogg, J. Kunkle, A. C. Mignerey, S. Nabil, F. Ricci-Tam, M. Seidel, Y. H. Shin, A. Skuja, S. C. Tonwar, K. Wong

Massachusetts Institute of Technology, Cambridge, USA
D. Abercrombie, B. Allen, A. Baty, R. Bi, S. Brandt, W. Busza, I. A. Cali, M. D’Alfonso, G. Gomez Ceballos, M. Goncharov, P. Harris, D. Hsu, M. Hu, M. Klute, D. Kovalskyi, Y.-J. Lee, P. D. Luckey, B. Maier, A. C. Marini, C. Meginn, C. Mironov, S. Narayanan, X. Niu, C. Paus, D. Rankin, C. Roland, G. Roland, Z. Shi, G. S. F. Stephens, K. Sumorok, K. Tat, D. Velicanu, J. Wang, T. W. Wang, B. Wyslouch

University of Minnesota, Minneapolis, USA
A. C. Benvenuti, R. M. Chatterjee, A. Evans, S. Guts, P. Hansen, J. Hiltbrand, Sh. Jain, S. Kalafut, Y. Kubota, Z. Lesko, J. Mans, R. Rusack, M. A. Wadud

University of Mississippi, Oxford, USA
J. G. Acosta, S. Oliveros

University of Nebraska-Lincoln, Lincoln, USA
K. Bloom, D. R. Claes, C. Fangmeier, L. Finco, F. Golf, R. Gonzalez Suarez, R. Kamalieddin, I. Kravchenko, J. E. Siado, G. R. Snow, B. Stieger

State University of New York at Buffalo, Buffalo, USA
C. Harrington, I. Iashvili, A. Kharchilava, C. Mclean, D. Nguyen, A. Parker, S. Rappoccio, B. Roozbahani

Northeastern University, Boston, USA
G. Alverson, E. Barberis, C. Freer, H. Haddad, A. Hortiangtham, G. Madigan, D. M. Morse, T. Orimoto, L. Skinnari, A. Tishelman-Charny, T. Wamorkar, B. Wang, A. Wisecarver, D. Wood

Northwestern University, Evanston, USA
S. Bhattacharya, J. Bueghly, T. Gunter, K. A. Hahn, N. Odell, M. H. Schmitt, K. Sung, M. Trovato, M. Velasco

University of Notre Dame, Notre Dame, USA
R. Bucci, N. Dev, R. Goldouzian, M. Hildreth, K. Hurtado Anampa, C. Jessop, D. J. Karmgard, K. Lannon, W. Li, N. Loukas, N. Marinelli, I. Mcalister, F. Meng, C. Mueller, Y. Musienko, M. Planer, R. Ruchti, P. Siddireddy, G. Smith, S. Taroni, M. Wayne, A. Wightman, M. Wolf, A. Woodard

The Ohio State University, Columbus, USA
J. Alimena, B. Bylsma, L. S. Durkin, S. Flowers, B. Francis, C. Hill, W. Ji, A. Lefeld, T. Y. Ling, B. L. Winer

Princeton University, Princeton, USA
S. Cooperstein, G. Dezoort, P. Elmer, J. Hardenbrook, N. Haubrich, S. Higginbotham, A. Kalogeropoulos, S. Kwan, D. Lange, M. T. Lucchini, J. Luo, D. Marlow, K. Mei, I. Ojalvo, J. Olsen, C. Palmer, P. Piroué, J. Salfeld-Nebgen, D. Stickland, C. Tully, Z. Wang
6: Also at Universidade Federal de Pelotas, Pelotas, Brazil
7: Also at Université Libre de Bruxelles, Bruxelles, Belgium
8: Also at University of Chinese Academy of Sciences, Beijing, China
9: Also at Institute for Theoretical and Experimental Physics, named by A.I. Alikhanov of NRC ‘Kurchatov Institute’, Moscow, Russia
10: Also at Joint Institute for Nuclear Research, Dubna, Russia
11: Also at Fayoum University, El-Fayoum, Egypt
12: Now at British University in Egypt, Cairo, Egypt
13: Also at Purdue University, West Lafayette, USA
14: Also at Université de Haute Alsace, Mulhouse, France
15: Also at Tbilisi State University, Tbilisi, Georgia
16: Also at Erzincan Binali Yıldırım University, Erzincan, Turkey
17: Also at CERN, European Organization for Nuclear Research, Geneva, Switzerland
18: Also at RWTH Aachen University, III. Physikalisches Institut A, Aachen, Germany
19: Also at University of Hamburg, Hamburg, Germany
20: Also at Brandenburg University of Technology, Cottbus, Germany
21: Also at Institute of Physics, University of Debrecen, Debrecen, Hungary
22: Also at Institute of Nuclear Research ATOMKI, Debrecen, Hungary
23: Also at MTA-ELTE Lendület CMS Particle and Nuclear Physics Group, Eötvös Loránd University, Budapest, Hungary
24: Also at IIT Bhubaneswar, Bhubaneswar, India
25: Also at Institute of Physics, Bhubaneswar, India
26: Also at Shoolini University, Solan, India
27: Also at University of Visva-Bharati, Santiniketan, India
28: Also at Isfahan University of Technology, Isfahan, Iran
29: Also at Italian National Agency for New Technologies, Energy and Sustainable Economic Development, Bologna, Italy
30: Also at Centro Siciliano di Fisica Nucleare e di Struttura Della Materia, Catania, Italy
31: Also at Università degli Studi di Siena, Siena, Italy
32: Also at Scuola Normale e Sezione dell’INFN, Pisa, Italy
33: Also at Riga Technical University, Riga, Latvia
34: Also at Malaysian Nuclear Agency, MOSTI, Kajang, Malaysia
35: Also at Consejo Nacional de Ciencia y Tecnología, Mexico City, Mexico
36: Also at Warsaw University of Technology, Institute of Electronic Systems, Warsaw, Poland
37: Also at Institute for Nuclear Research, Moscow, Russia
38: Also at National Research Nuclear University 'Moscow Engineering Physics Institute' (MEPhI), Moscow, Russia
39: Also at St. Petersburg State Polytechnical University, St. Petersburg, Russia
40: Also at University of Florida, Gainesville, USA
41: Also at Imperial College, London, UK
42: Also at P.N. Lebedev Physical Institute, Moscow, Russia
43: Also at Budker Institute of Nuclear Physics, Novosibirsk, Russia
44: Also at Faculty of Physics, University of Belgrade, Belgrade, Serbia
45: Also at INFN Sezione di Pavia a, Università di Pavia b, Pavia, Italy
46: Also at National and Kapodistrian University of Athens, Athens, Greece
47: Also at Universität Zürich, Zurich, Switzerland
48: Also at Stefan Meyer Institute for Subatomic Physics, Vienna, Austria
49: Also at Gaziosmanpasapa University, Tokat, Turkey
50: Also at Şırnak University, Şırnak, Turkey
51: Also at Beykent University, Istanbul, Turkey
52: Also at Istanbul Aydin University, Application and Research Center for Advanced Studies (App. & Res. Cent. for Advanced Studies), Istanbul, Turkey
53: Also at Mersin University, Mersin, Turkey
54: Also at Piri Reis University, Istanbul, Turkey
55: Also at Adiyaman University, Adiyaman, Turkey
56: Also at Ozyegin University, Istanbul, Turkey
57: Also at Izmir Institute of Technology, Izmir, Turkey
58: Also at Marmara University, Istanbul, Turkey
59: Also at Kafkas University, Kars, Turkey
60: Also at Istanbul University, Istanbul, Turkey
61: Also at Istanbul Bilgi University, Istanbul, Turkey
62: Also at Hacettepe University, Ankara, Turkey
63: Also at School of Physics and Astronomy, University of Southampton, Southampton, UK
64: Also at IPPP Durham University, Durham, UK
65: Also at Monash University, Faculty of Science, Clayton, Australia
66: Also at Bethel University, St. Paul, Minneapolis, USA, St. Paul, USA
67: Also at Karamanoğlu Mehmetbey University, Karaman, Turkey
68: Also at Vilnius University, Vilnius, Lithuania
69: Also at Bingol University, Bingol, Turkey
70: Also at Georgian Technical University, Tbilisi, Georgia
71: Also at Sinop University, Sinop, Turkey
72: Also at Mimar Sinan University, Istanbul, Istanbul, Turkey
73: Also at Texas A&M University at Qatar, Doha, Qatar
74: Also at Kyungpook National University, Daegu, Korea, Daegu, Korea
75: Also at University of Hyderabad, Hyderabad, India