E(5) and X(5) shape phase transitions within a Skyrme Hartree-Fock + BCS approach

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(Dated: February 2, 2008)

Self-consistent Skyrme Hartree-Fock plus BCS calculations are performed to generate potential energy curves (PEC) in various chains of Pd, Xe, Ba, Nd, Sm, Gd, and Dy isotopes. The evolution of shapes with the number of nucleons is studied in a search for signatures of E(5) and X(5) critical point symmetries. It is shown that the energy barriers in the PECs are determined to a large extent by the treatment of the pairing correlations.

PACS numbers: 21.60.Jz, 21.60.Fw, 27.60.+j, 27.70.+q

I. INTRODUCTION

The ground states of atomic nuclei are characterized by different equilibrium configurations which correspond to different geometrical shapes. The study of these equilibrium shapes, as well as the transition regions between them, has been the subject of a large number of theoretical and experimental studies (for a review, see, for example, Ref. [1] and references therein).

Within the framework of algebraic models, the different nuclear phase shapes are put in correspondence to dynamic symmetries of some algebraic structure that links a specific mathematical symmetry with a specific nuclear shape. Dynamic symmetries provide a useful tool to describe properties of different physical systems since they lead to exactly solvable problems and produce all results for observables in explicit analytic form.

In nuclear physics, the algebraic structure of relevance, according to the Interacting Boson Model (IBM) [2], is given by U(6). There are three dynamical symmetries characterized by U(5), associated to spherical symmetry, SU(3), associated with axially deformed symmetry, and SO(6), describing γ-unstable shapes. Experimental examples of all three types of symmetries have been recognized in many nuclei.

The phase shape transitions correspond to the breaking of these dynamic symmetries and they occur as the number of nucleons change in the nucleus. Understanding the behavior of systems undergoing a phase transition is of especial relevance, since a complicated interplay of competing degrees of freedom occurs at the critical points.

Iachello [3, 4] introduced the E(5) and X(5) critical point symmetries within the framework of the collective Bohr Hamiltonian [2] under some simplifying approximations. Critical point symmetries provide parameter free (up to scale factors) predictions of excitation spectra and electric quadrupole B(E2) strengths for nuclei at the critical point of a phase/shape transition. The geometrical shape of the ground state can be described by three Euler angles and by the quadrupole deformation parameters β and γ. At the critical point of the phase transition the potential in the β degree of freedom can be approximated by a simple square well potential, which is decoupled from the potential in the γ-variable.

In the case of the E(5) critical point symmetry, which corresponds to the transition from spherical vibrational U(5) to deformed γ-unstable O(6), the potential is flat in the γ-direction. In the case of the symmetry X(5), related to the transition from U(5) to axially symmetric prolate SU(3), a harmonic oscillator potential is used in the γ-direction.

Empirical evidence of these transitional symmetries at the critical points were soon found in 134Ba [6] for E(5) and in 152Sm [7] for X(5). Other nuclei have also been identified as good candidates for those symmetries. Such is the case of 102Pd [8], and 128-130Xe [9], which provide examples of E(5) symmetry. Other N=90 isotones like 150Nd [10], 154Gd [11], and 156Dy [12] also provide examples of X(5) symmetry.

Algebraic models are very suitable for systematic studies because they provide powerful predictions with a very small number of parameters, but in order to deepen into the details, one has to perform microscopic investigations of shape transitions and critical points which are, to a large extent, still missing. In particular, it is interesting to examine whether the assumptions of relatively flat potentials in E(5) and X(5) are justified in different microscopic models and the self-consistent mean-field approximation, based on parametrizations widely used all over the nuclear chart, appears as a very attractive initial tool for a link between algebraic models and microscopic theories. In this context, the relativistic mean-field framework has been employed, in calculations of PECs as functions of the quadrupole deformation [13, 14, 15]. These studies have been performed for isotopic chains in which the occurrence of critical point symmetries has been predicted. Since flat PECs are one of the expected characteristics of critical point symmetries, constrained calculations in those isotopic chains should result in relatively flat PECs for nuclei with the critical symmetry. It has been shown that particular isotopes exhibit relatively flat PECs over an extended range of the deformation parameter. Nevertheless, the behavior of the PECs, and particularly the potential barriers, are quite sensitive to

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the relativistic interaction used\[13\], as well as to the pair-
ing treatment. Therefore, the question arises whether a
similar situation occurs when using nonrelativistic effec-
tive interactions to study candidates for critical point
symmetries. Such systematic nonrelativistic studies are
still missing and it is very interesting to compare the con-
clusions extracted from them with those obtained using
both algebraic models and relativistic mean-field approx-
imations.

In this work, we extend the calculations mentioned
above to the case of nonrelativistic self-consistent Skyrme
Hartree-Fock + BCS mean-field calculations. The shape
phase transitions corresponding to E(5) and X(5) sym-
metries are investigated systematically in various isotopic
chains containing some of the suggested critical nuclei.
In particular we study Pd, Xe, and Ba isotopic chains as
candidates to E(5) symmetry, and Nd, Sm, Gd, and Dy
isotopic chains as examples of X(5).

The paper is organized as follows. In Sec. II we present
a brief description of the theoretical formalism (Hartree-
Fock + BCS) used to obtain the main ingredient of the
present study, i.e., the PECs for the considered isotopic
chains. For a more detailed account the reader is referred
to the corresponding literature. Sec. III contains our
results with a discussion on the sensitivity of the PECs to
the effective nucleon-nucleon force and to the treatment
of the pairing correlations. Sec. IV is devoted to the
concluding remarks.

II. THEORETICAL FRAMEWORK

The microscopic approach used in this work (i.e.,
HF+BCS) is based on a self-consistent formalism built on
a deformed Hartree-Fock (HF) mean-field, using Skyrme
type energy density functionals. Pairing correlations be-
tween like nucleons are included in the BCS approxi-
mation. It is well known that the density-dependent
HF+BCS approximation provides a very good description
of ground-state properties for both spherical and
deformed nuclei\[16\] and it is at present one of the state-
of-the-art mean-field descriptions\[17\].

There are two leading choices of methods to solve the
deformed HF+BCS equations. One option is the use
of a coordinate space mesh. In this case one solves
the HF+BCS equations for Skyrme type functionals via
discretization of the individual wave functions on a 3-
dimensional cartesian mesh\[18\]. This corresponds to an
expansion on a specific basis of Lagrange polynomials
associated with the selected mesh. The other common
choice is to expand the single particle wave functions into
an appropriate orthogonal basis (commonly the eigen-
fuctions of an axially symmetric harmonic oscillator po-
tential). In the present study we perform calculations
with both methods. We use the code ev8\[18\] in the first
case and follow the procedure based on the formalism
developed in Ref.\[13\] in the second case.

In this work we consider the parametrization SLy4\[20\]
of the Skyrme force in the particle-hole channel, although
we also show results in some instances for the forces Sk3
\[21\] and SG2\[22\]. They are examples of global effec-
tive interactions of Skyrme-type that have been designed
to fit ground state properties of spherical nuclei and nu-
clear matter properties. While Sk3 is the most simple
one, involving in particular a linear dependence on the
density, SLy4 is one of the most recent parametrizations
of Skyrme forces.

As we move away from closed shells, pairing correla-
tions play an important role\[23\] and should be taken into
account. If one were dealing with a fundamental many-
body Hamiltonian, one would proceed to apply Hartree-
Fock-Bogoliubov formalism to it. However, dealing with
Skyrme forces that have been simplified with the aim of
reproducing average or bulk properties of the nucleus,
one would have to include additional parameters in or-
der to guarantee that sensible pairing matrix elements
are obtained\[17,18\].
In this study pairing correlations are taken into account in the BCS approximation. Several options have been investigated. Our main option will be the use of a zero-range density-dependent pairing force [24],

$$V(r_1, r_2) = -g \left(1 - \hat{P}^\sigma \right) \left(1 - \frac{\rho(r_1)}{\rho_c} \right) \delta(r_1 - r_2),$$  \hspace{1cm} (1)

where \(\hat{P}^\sigma\) is the spin exchange operator, \(\rho(r)\) is the nuclear density, and \(\rho_c = 0.16 \text{ fm}^{-3}\). The strength \(g\) of the pairing force [Eq.(1)] is taken to be \(1000 \text{ MeV-fm}^3\) for both neutrons and protons and a smooth cut-off of 5 MeV around the Fermi level has also been used. Let us mention that very recently the parametrization SLy4 has been successfully applied in combination with the pairing interaction [Eq. (1)] (with \(g = 1000 \text{ MeV-fm}^3\)) in systematic studies of correlation energies from \(^{16}\text{O}\) to the super-heavy elements [25] and in global studies of spectroscopic properties of the first \(2^+\) states in even-even nuclei [26]. This is the main reason for selecting the combination SLy4 in the particle-hole channel and the interaction [Eq. (1)] (with \(g = 1000 \text{ MeV-fm}^3\)) in the pairing channel as the leading choice for the present study. Additionally, results with the strength \(g = 1250 \text{ MeV-fm}^3\) will also be shown in some cases.

Another common practice to include pairing correlations is to introduce a schematic seniority pairing force with a constant pairing strength \(G\) [24], called this treatment constant-force approach,

$$V_{pair} = -G \sum_{m, m'} a_m^\dagger a_{m'}^\dagger \Delta_{p,n},$$  \hspace{1cm} (2)

The strength of the pairing force for protons and neutrons \(G_{p,n}\) is chosen in such a way that the experimental pairing gaps extracted from binding energies in neighboring nuclei are reproduced. One can further simplify the pairing treatment by parametrizing the pairing gaps \(\Delta_{p,n}\) directly from experiment, we call this treatment constant-gap approach. The pairing strength and pairing gap are related through the gap equation [23]

$$\Delta = G \sum_{\nu > 0} u_{\nu} v_{\nu},$$  \hspace{1cm} (3)

where \(v_{\nu}\) are the occupation amplitudes.

The PECs shown in this study are computed microscopically by constrained HF+BCS calculations [18, 23, 27]. These PECs are obtained by minimizing the corresponding energy functional under a quadratic constraint that holds the nuclear quadrupole moment fixed to a given value. In this work we show the energies as a function of the (axially symmetric) mass quadrupole moment \(Q\), which is related with the quadrupole deformation parameter \(\beta_2\) by the expression

$$\beta_2 = \sqrt{\frac{\pi}{5}} \frac{Q}{A < r^2 >},$$  \hspace{1cm} (4)

in terms of the mean square radius of the mass distribution \(< r^2 >\). Tables I and II contain the quadrupole parameters \(\beta_2\) corresponding to the equilibrium configurations for the isotopes considered in this work.

| 
| \(\text{Pd}\) | \(\text{Xe}\) | \(\text{Ba}\) |
|---|---|---|
| \(g=1000\) | \(\text{g=1000}\) | \(\text{g=1000}\) |
| \(\text{g=1250}\) | \(\text{g=1250}\) | \(\text{g=1250}\) |

TABLE I: Quadrupole deformation parameters \(\beta_2\) for the ground states in Pd, Xe, and Ba isotopes. SLy4 force and two values of the pairing strength \(g\) \([\text{MeV-fm}^3]\) are used.

III. DISCUSSION OF RESULTS

It is known that PECs are sensitive to the effective nuclear force in both relativistic [13] and nonrelativistic [28, 29] approaches, as well as to pairing correlations [28, 29]. Thus, it is worth starting our discussion on PECs by studying this sensitivity in our case. We perform this study on the example of \(^{128}\text{Xe}\) and \(^{152}\text{Sm}\), which are proposed candidates for E(5) and X(5) symmetries, respectively.

In Fig. 3 we study the effect of using different methods of solving the HF+BCS equations, coordinate lattice [18] and deformed harmonic oscillator basis [19]. In these calculations we use the same SLy4 force in the particle-hole

FIG. 3: Potential energy curves obtained with different treatments of pairing. For details see the main text.
TABLE II: Quadrupole deformation parameters $\beta_2$ for the ground states in Nd, Sm, Gd, and Dy isotopes. SLy4 force and pairing strength $g=1000$ [MeV fm$^3$] are used.

| Element | 142 | 144 | 146 | 148 | 150 | 152 | 154 | 156 |
|---------|-----|-----|-----|-----|-----|-----|-----|-----|
| Nd      | 0.00 | 0.10 | 0.14 | 0.20 | 0.28 | 0.29 | 0.29 | 0.30 |
| Sm      | 144 | 146 | 148 | 150 | 152 | 154 | 156 | 158 |
| Gd      | 146 | 148 | 150 | 152 | 154 | 156 | 156 | 156 |
| Dy      | 148 | 150 | 152 | 154 | 156 | 156 | 158 | 158 |

The results indicate that the PECs obtained are practically the same in these two cases and in general in all the isotopes we have considered in this work.

In Fig. 2 we consider the PECs obtained from three different Skyrme forces, namely SLy4, SG2, and Sk3, using the same pairing treatment. We can see that the location of the oblate and prolate minima appear at the same deformation no matter what the force is. However, the relative energies of the minima and the energy barriers between the minima can change by a few MeV, depending on the force.

In Fig. 3 we show the effect of pairing using SLy4 force in all cases. We consider the constant-gap approach and the constant-force approach. Again, we observe that the minima appear at about the same deformations but the energy barriers can change considerably depending on the approach used.

From the analysis of Figs. 1, 2 and 3 we conclude that, at least in the mass region studied, the PECs are not sensitive to the method employed to solve the HF+BCS equations (3D cartesian lattice or deformed harmonic oscillator). We also conclude that the qualitative behavior of the energy profiles remains unchanged against changes in the Skyrme and pairing interactions in the sense that the deformations at which the minima occur are rather stable. Nevertheless, the relative energies of these minima, and particularly the energy barriers between them are very sensitive to the details of the calculation, especially to pairing. This is also the case in relativistic mean-field calculations. The sensitivity of the PECs to the force can be seen in Ref. [13], where several forces were compared (NL1, NL3, NLSh, and TM1). The sensitivity to the pairing in relativistic calculations is also apparent if one compares the energy barriers in Sm isotopes obtained with the parametrization NL3 in Ref. [13], where a constant-gap approach was used, with those in Ref. [13], where a pairing based on the Brink-Boeker part of the Gogny force was used. One should remark that, at variance with Ref. [13], a self-consistent treatment of the pairing is used in Ref. [13]. The main effect is a reduction of the energy barriers in the self-consistent treatment. In the case of nonrelativistic calculations with the Gogny interaction, since the same force is used in both mean-field and pairing channels, a fully self-consistent treatment is possible within a Hartree-Fock-Bogoliubov formalism. It will be very interesting to explore whether this reduction of the barriers is also present. Work along this line is in...
progress.

To appreciate the effect on the energy barriers in more detail, we show in Figs. 4, 5, and 6 the results for PECs in $^{96-114}\text{Pd}$, $^{118-136}\text{Xe}$, and $^{120-138}\text{Ba}$ isotopic chains, respectively. The quadrupole deformations corresponding to the ground states of these isotopes can be found in Table I. These chains contain E(5) candidates found from systematic studies on available data on energy levels, E2, E1, and M1 strengths [6, 8, 9, 30, 31].

The PECs shown in Figs. 4, 5, and 6 have been computed within the mean-field scheme based on the Paris-Brussels code ev8, using the parametrization SLy4 and two different choices of the strength $g$ of the zero-range pairing force [Eq. (1)], $g = 1000$ MeV-fm$^3$ and $g = 1250$ MeV-fm$^3$. From these figures one can see once more that oblate and prolate minima do not change significantly with the strength of pairing in each isotope. The only exceptions worth to mention are the cases $^{96}\text{Pd}$, $^{114}\text{Pd}$,
and $^{134}$Xe, where we obtain the ground state at different deformations depending on the pairing strength $g$. This happens because of the flatness of the corresponding PECs, but in any case the energy difference between the minima are always very small. On the other hand, the potential barriers are clearly lower when pairing is stronger.

We can also observe the transition from the spherical isotopes $^{96}$Pd ($N=50$), $^{136}$Xe ($N=82$), and $^{138}$Ba ($N=82$) to the $\gamma$-unstable isotopes $^{114}$Pd, $^{118}$Xe, and $^{120}$Ba. We identify the isotopes $^{108,110}$Pd, $^{128,130}$Xe, and $^{130,132}$Ba as transitional nuclei with rather flat PECs (especially with $g=1250$). These results confirm the assumed square well potential in the $\beta$ degree of freedom that leads to the critical point symmetry $E(5)$. They are also in good agreement with the results obtained in Ref. [15] using the parametrization NL3 of the relativistic mean-field Lagrangian and a pairing force based on the Brink-Boeker part of the Gogny interaction.

Fig. 7 shows the evolution of the energy barriers as a function of the number of neutrons for Xe isotopes for the two values of the pairing strength $g = 1000$ MeV-fm$^3$ and $g = 1250$ MeV-fm$^3$ in [Eq.(1)]. As it can be observed, the barriers obtained with the strength $g = 1250$ MeV-fm$^3$ are systematically lower than the ones obtained with $g = 1000$ MeV-fm$^3$.

Now we turn the discussion to several rare-earth isotopic chains, Nd, Sm, Gd, and Dy, where some of the nuclei ($N=90$ isotones) have been identified as exhibiting X(5) behavior, a transition between a spherical shape and a well deformed prolate shape. For example, the nucleus $^{152}$Sm [7] was the first identified as exhibiting X(5) behavior and this is also the case for $^{150}$Nd [10]. Other candidates have also been suggested with further work (see, for example, Refs. [32, 33, 34]).

Fig. 8 shows the results for $^{142−156}$Nd isotopes (Z=60). The corresponding ground state deformation parameters for these nuclei are given in Table II. We can observe a clear shape transition from spherical $^{142}$Nd ($N=82$) to clearly prolate $^{152−156}$Nd. The isotopes $^{148}$Nd ($N=88$) and $^{150}$Nd ($N=90$) show a transitional behavior with a rather flat minimum on the prolate side and additional minima on the oblate sector at 3 MeV and 4 MeV excitation energy, respectively. The energy barrier is about 5 MeV in $^{148}$Nd and 8 MeV in $^{150}$Nd.

Fig. 9 contains the PECs for $^{144−158}$Sm isotopes (Z=62). The corresponding ground state deformation parameters are given in Table II. Similar arguments to
those in Nd are valid. The transitional behavior between spherical, $^{144}$Sm, and well prolate deformed, $^{154−158}$Sm, appears again for the N=88 and N=90 isotopes, $^{150}$Sm and $^{152}$Sm, respectively. The energy barriers and energy differences between oblate and prolate minima in Sm isotopes are shown in Fig. 10. They are qualitatively similar to the barriers obtained in the other rare-earth isotopic chains. Our PECs for $^{144−158}$Sm agree qualitatively with those of Refs. [13] and [15]. They also agree well with the results obtained in Ref. [35] with the Nilsson-Strutinsky + BCS calculations.

The same is true for Gd and Dy isotopes, whose PECs are shown in Figs. 11 and 12, respectively. The ground state deformation parameters for the considered Gd and Dy isotopes are given in Table II. In this case, we find the transitional behavior for $A=152,154$ in Gd isotopes and $A=154,156$ for Dy isotopes.

From the results described above we conclude that our calculations do not predict flat PECs for the N=90 isotopes, in agreement with previous studies (see, for example, Ref. [15]).

### IV. CONCLUSIONS

In this paper we have investigated the potential energy curves in a series of isotopic chains containing transitional nuclei that exhibit a critical point symmetry behavior. A microscopic approach based on deformed HF+BCS calculations with Skyrme forces has been used.

We have studied the sensitivity of our results to the effective nucleon-nucleon interaction and to the pairing force. From this analysis we conclude that the energy barriers in the PECs depend strongly on the details of calculations, especially on the pairing force. This is indeed relevant for this work because our purpose is to study up to what extent the PECs exhibit a flat behavior at the critical point symmetries.

We have found that the assumptions of flat potentials in the E(5) critical point symmetry is supported by the present microscopic calculations in $^{108,110}$Pd, $^{128,130}$Xe, and $^{130,132}$Ba, that have been suggested as examples of E(5). In the case of X(5) we find that the rare-earth isotopes with N=88,90 show a transitional behavior that could be interpreted in terms of X(5) symmetry. However, we do not find a flat behavior, in agreement with previous calculations [13, 14, 15].

There remains a long list of tasks to be undertaken in the near future but the present study could be considered as a first step into a much more systematic exploration of the relation between algebraic models and (nonrelativistic) microscopic models. In particular, it is very important to understand how well the predictions of effective...
interactions with predictive power all over the nuclear chart compare with those of the already mentioned algebraic models.

Acknowledgments

This work was partly supported by Ministerio de Educación y Ciencia (Spain) under Contract No. FIS2005–00640. One of us (R.R.) would like to thank Prof. F. Iachello (Yale University) for valuable suggestions and discussions.

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