Model-based reconstruction for simultaneous multi-slice $T_1$ mapping using single-shot inversion-recovery radial FLASH

Xiaoqing Wang$^{1,2}$ | Sebastian Rosenzweig$^{1,2}$ | Nick Scholand$^{1,2}$ | H. Christian M. Holme$^{1,2}$ | Martin Uecker$^{1,2,3,4}$

$^1$Institute for Diagnostic and Interventional Radiology, University Medical Center Göttingen, Göttingen, Germany
$^2$German Centre for Cardiovascular Research (DZHK), Partner Site Göttingen, Göttingen, Germany
$^3$Cluster of Excellence “Multiscale Bioimaging: from Molecular Machines to Networks of Excitable Cells” (MBExC), University of Göttingen, Göttingen, Germany
$^4$Campus Institute Data Science (CIDAS), University of Göttingen, Göttingen, Germany

Correspondence
Xiaoqing Wang, Institute for Diagnostic and Interventional Radiology of the University Medical Center Göttingen, Robert-Koch-Str. 40, 37075 Göttingen, Germany. Email: xiaoqing.wang@med.uni-goettingen.de, Twitter: @xqwang1

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Purpose: To develop a single-shot multi-slice $T_1$ mapping method by combing simultaneous multi-slice (SMS) excitations, single-shot inversion-recovery (IR) radial fast low-angle shot (FLASH), and a nonlinear model–based reconstruction method.

Methods: SMS excitations are combined with a single-shot IR radial FLASH sequence for data acquisition. A previously developed single-slice calibrationless model–based reconstruction is extended to SMS, formulating the estimation of parameter maps and coil sensitivities from all slices as a single nonlinear inverse problem. Joint-sparsity constraints are further applied to the parameter maps to improve $T_1$ precision. Validations of the proposed method are performed for a phantom and for the human brain and liver in 6 healthy adult subjects.

Results: Phantom results confirm good $T_1$ accuracy and precision of the simultaneously acquired multi-slice $T_1$ maps in comparison to single-slice references. In vivo human brain studies demonstrate the better performance of SMS acquisitions compared to the conventional spoke-interleaved multi-slice acquisition using model-based reconstruction. Aside from good accuracy and precision, the results of 6 healthy subjects in both brain and abdominal studies confirm good repeatability between scan and re-scans. The proposed method can simultaneously acquire $T_1$ maps for 5 slices of a human brain ($0.75 \times 0.75 \times 5 \text{ mm}^3$) or 3 slices of the abdomen ($1.25 \times 1.25 \times 6 \text{ mm}^3$) within 4 seconds.

Conclusions: The IR SMS radial FLASH acquisition together with a nonlinear model–based reconstruction enable rapid high-resolution multi-slice $T_1$ mapping with good accuracy, precision, and repeatability.

Keywords
$T_1$ mapping, model-based reconstruction, radial FLASH, simultaneous multi-slice
INTRODUCTION

Quantitative mapping of MR relaxation times such as $T_1$ finds increasing applications in a variety of clinical use cases.\(^1,2\) Mapping of $T_1$ relaxation time commonly relies on the inversion-recovery (IR) Look-Locker sequence where RF excitations are continuously applied after inversion followed by computation of a $T_1$ map in a postprocessing step.\(^3-5\) While efficient, the conventional IR Look-Locker method may still require segmented data acquisitions with multiple inversions.\(^4,5\) As a sufficient delay is necessary between inversions, these techniques still suffer from long measurement time. Most recently, advances in sequence development such as non-Cartesian sampling together with state-of-the-art reconstruction techniques have enabled faster parameter mapping,\(^6-13\) including accelerated $T_1$ mapping within a single inversion recovery.\(^14-16\) These methods usually consist of 2 steps: First, reconstruction of contrast-weighted images from undersampled datasets, and second, subsequent voxel-by-voxel fitting of the $T_1$ map. In contrast, nonlinear model–based reconstruction methods\(^6,17-26\) estimate parameter maps directly from $k$-space, completely bypassing the intermediate step of image reconstruction and voxel-by-voxel fitting. Moreover, a priori information such as sparsity constraints can be applied to the parameter maps to improve precision.\(^6,20,22,25\)

So far, most of the above efforts have focused on the acceleration of single-slice parameter mapping. However, in clinical applications, multi-slice parameter mapping is highly desirable. For example, it has been recommended to perform myocardial $T_1$ mapping in at least 3 short-axis sections to capture potential heterogeneity across the left ventricular wall.\(^27,28\) Methods exploiting the conventional multi-slice acquisition strategy have been reported.\(^29-32\) In contrast, the simultaneous multi-slice (SMS) technique\(^33\) is a promising way to accelerate multi-slice quantitative MRI. SMS allows for the distribution of undersampling along the additional slice dimension and exploits sensitivity encoding in all 3 spatial dimensions. Applications of SMS in quantitative MRI include but are not limited to simultaneous 3-slice MR fingerprinting,\(^34\) simultaneous 3-slice cardiac $T_1$ mapping based on the SAPPHIRE technique\(^28\) and simultaneous multi-slice $T_2$ mapping using the Cartesian multi-echo spin-echo sequence with a model-based iterative reconstruction.\(^35\)

To further enable fast $T_1$ mapping of multiple slices, in this work, we aim to combine simultaneous multi-slice excitations and single-shot IR radial FLASH with a nonlinear model–based reconstruction to enable multi-slice $T_1$ mapping within a single inversion recovery. In particular, we first combine SMS excitation with the single-shot IR radial FLASH sequence using a golden-angle readout. Next, we extend a previously developed single-slice calibrationless model–based reconstruction to SMS, formulating the estimation of parameter maps and coil sensitivities from all slices as a single nonlinear inverse problem. In this way, no additional coil-calibration steps are needed. Furthermore, joint-sparsity constraints are applied on the parameter maps to improve $T_1$ precision. Performance of the proposed method is validated first on an experimental phantom and then on human brain and liver studies of 6 healthy adult subjects.

METHODS

2.1 Sequence design

The sequence starts with a nonselective adiabatic inversion pulse, followed by a radial FLASH readout using continuous SMS excitations and a tiny golden angle between successive spokes ($\approx 23.63^\circ$).\(^36\) In the partition dimension, radial spokes can be designed to follow an aligned or nonaligned distribution as shown in Figure 1. The aligned scenario allows decoupling of SMS data using an inverse Fourier transform along the partition dimension, followed by independent reconstruction of each slice. In such a way, there is still the SNR benefit of a SMS acquisition over the spoke-interleaved multi-slice scheme. However, the main advantage of SMS—acceleration in the direction perpendicular to the slices—only comes into play when distinct $k$-space samples are acquired in each partition.\(^37,38\) Figure 1 (bottom) depicts the latter case, where a larger $k$-space coverage could be achieved within a given readout time. In this work, we applied the tiny golden angle ($\approx 23.63^\circ$) sampling in the partition dimension as well. Accordingly, throughout this manuscript, we adopt the terms “SMS aligned” and “SMS golden-angle” to refer to the two SMS acquisition strategies, respectively. To reconstruct images/parameter maps in the latter SMS golden-angle acquisition scheme, conventional slice-by-slice reconstruction cannot be used. A more general SMS model-based reconstruction method is therefore developed, which is explained in the following.

2.2 SMS model–based reconstruction

Following a similar notation introduced in,\(^38\) we define $p, q \in \{1, \ldots, Q\}$ as the partition index and the slice index, respectively, where $Q$ is the total number of partitions/slices. In SMS acquisitions, the signal from the $p$th partition $\vec{y}$ can be written as

$$\vec{y} = \sum_{q=1}^{Q} \varphi^p \cdot \vec{y}_q,$$

(1)
where $\varphi_{p,q}$ is an SMS encoding matrix. In this study, it is chosen as the Fourier matrix, that is, 
\[ \varphi_{p,q} = \exp \left( -2\pi i \frac{p+1}{Q} \right) \]. The signal $y_j^q(t)$ for the $q$th slice of the $j$th coil is given by 
\[ y_j^q(t) = \int M^q(\tilde{r}) e^{i\varphi_{p,q}(\tilde{r})} e^{-\tilde{t}_k(t)} d\tilde{r}, \]
where $e^q$ is the corresponding coil sensitivity map, $\tilde{r}$ is the position in image space, and $\tilde{t}_k(t)$ is the chosen k-space trajectory. $M^q$ is the $T_1$ relaxation model for the $q$th slice at the inversion time $t_k$:
\[ M^q_{t_k} = M^q_{ss} - (M^q_{ss} + M^q_0) \cdot e^{-t_k R_1^q}, \]
where $t_k$ is defined as the center of each acquisition window. $M^q_{ss}$, $M^q_0$, and $R_1^q$ are the steady-state signal, equilibrium signal, and effective relaxation rate, respectively. After estimation of $(M^q_{ss}, M^q_0, R_1^q)$, $T_1$ values of the $q$th slice can be calculated by $T_1^q = \frac{M^q_{ss}}{M^q_0 + 2 \cdot \delta t}$, with $\delta t$ the delay between inversion and the start of data acquisition, which is around 15 ms for the sequence used in this study. To estimate parameter maps and coil sensitivity maps from all slices, Equations (1) and (2) are understood as a nonlinear inverse problem with a nonlinear operator $F$, mapping all the unknowns from all slices to the measured undersampled SMS data $Y = (\hat{y}_1^1, \ldots, \hat{y}_1^q, \ldots, \hat{y}_N^q)^T$:
\[ F : x \mapsto P \Xi = \begin{pmatrix} F(e^1 \cdot M^q_{t_1}) \\ \vdots \\ F(e^N \cdot M^q_{t_q}) \end{pmatrix}, \]
with $P \Xi = \begin{pmatrix} P_{1,x}^y & 0 \\ \vdots \\ 0 & P_{N,x}^y \end{pmatrix}$, where $P_{N,x}^y$ is the sampling operator for the given k-space trajectory and $F$ is the 2-dimensional Fourier transform.

$e^q$ represents a set of coil sensitivity maps for the $q$th
slice. \( M^q_{sl}(-) \) is the relaxation model described in Equation (3). The unknowns are \( x = (x^1, \ldots, x^q, \ldots, x^{Q})^T \) with \( x^q = (M^q_{m1}, M^q_{m2}, R^q_1, c^q_1, \ldots, c^q_M)^T \), which are then estimated by solving the following regularized nonlinear inverse problem:

\[
\hat{x} = \arg\min_{x \in D} \| F(x) - \hat{y} \|_2^2 + \alpha \sum_{q=1}^{Q} R(x^q_m) + \beta \sum_{q=1}^{Q} U(x^q) , \quad (6)
\]

with \( R(\cdot) \) the joint \( \ell^r \)-Wavelet regularization in the parameter dimension \(^{25} \) and \( U(\cdot) \) the Sobolev norm \(^{39} \) enforcing the smoothness of coil sensitivity maps. \( x^q_m = (M^q_{m1}, M^q_{m2}, R^q_1)^T \) and \( x^q = (c^q_1, \ldots, c^q_M)^T \), \( \alpha \) and \( \beta \) are the regularization parameters for the parameter and coil-sensitivity maps, respectively. \( D \) is a convex set ensuring \( R^q_1 \) to be nonnegative. The above nonlinear inverse problem is then solved by the iteratively regularized Gauss-Newton method (IRGNM) where in each Gauss-Newton step the nonlinear problem is linearized and solved by the fast iterative shrinkage-thresholding algorithm (FISTA). \(^{40} \) More details on the IRGNM-FISTA algorithm can be found in ref\(^{25} \).

### 2.3 | Data acquisition

All MRI experiments were conducted on a Magnetom Skyra 3T (Siemens Healthineers, Erlangen, Germany) with approval of the local ethics committee. The proposed method was first validated on a commercial reference phantom (Diagnostic Sonar LTD, Scotland, UK) consisting of 6 compartments with defined \( T_1 \) values surrounded by water. Phantom and brain studies were conducted with a 20-channel head/neck coil, whereas abdominal scans were performed with a combined thorax and spine coil with 26 channels. Six subjects (4 females and 2 males, 26 ± 5 years old) without known illness were recruited. For each subject, both brain and liver measurements were performed. In all experiments, simultaneously acquired slices using IR radial FLASH are separated by a fixed distance \( d \). All single-slice and multi-slice acquisitions employed the same nominal flip angle \( \alpha = 6^\circ \). Acquisition parameters for phantom and brain measurements were: FOV: \( 192 \times 192 \text{ mm}^2 \), matrix size: \( 256 \times 256 \), TR/TE = 4.10/2.58 ms, bandwidth 630 Hz/pixel, slice thickness \( \Delta z = 5 \text{ mm} \), slice distances \( d = 15 \text{ mm} \) and \( d = 20 \text{ mm} \) for phantom and in vivo studies, respectively. A gold standard \( T_1 \) mapping was performed on the center slice of the phantom using an IR spin-echo method \(^{41} \) with 9 IR scans (\( TI = 30, 530, 1030, 1530, 2030, 2530, 3030, 3530, \) and 4030 ms), TR/TE = 4050/12 ms, FOV: \( 192 \times 192 \text{ mm}^2 \), matrix size: \( 192 \times 192 \), and a total acquisition time of 2.4 hours. Parameters for the abdominal measurements were: FOV: \( 320 \times 320 \text{ mm}^2 \), matrix size: \( 256 \times 256 \), TR/TE = 2.70/1.69 ms, bandwidth 850 Hz/pixel, \( \Delta z = 6 \text{ mm} \), \( d = 20 \) mm. All single-shot measurements were acquired within a 4-second duration, which was chosen to compromise between good \( T_1 \) accuracy, SNR while still keep the acquisition time short. \(^{15} \) The SMS golden-angle acquisitions were executed twice to evaluate the repeatability of the proposed method. Abdominal experiments were performed during a brief breathhold.

### 2.4 | Numerical implementation

All SMS image reconstruction was done offline based on the software package BART\(^{42} \) using a 40-core 2.3 GHz Intel Xeon E5-2650 server with a RAM size of 512 GB. For abdominal studies, coil elements far away from the regions of interest (ie, coils near the arm regions) were manually excluded to image reconstruction to remove residual streaking artifacts. \(^{43} \) After gradient-delay correction \(^{44} \) and channel compression to 8 principle components, the multi-coil radial raw data were gridded onto a Cartesian grid, where all successive iterations were then performed using FFT-based convolutions with the point-spread function. \(^{45,46} \) Parameter maps \( (M^q_{ss}, M^q_{01}, R^q_1)^T \) were initialized with \( (1.0, 1.0, 2.0)^T \) and all coil sensitivities were initialized with zeros for all slices. The regularization parameters \( \alpha \) and \( \beta \) were initialized with 1.0 and subsequently reduced by a factor of 3 in each Gauss-Newton step. A minimum value of \( \alpha \) was used to control the noise of the estimated parameter maps even with a larger number of Gauss-Newton steps. The optimal value \( \alpha_{\text{min}} \) was chosen manually to optimize SNR without compromising the quantitative accuracy or delineation of structural details. Ten Gauss-Newton steps were employed to ensure convergence. With these settings, it took around 10 hours to reconstruct a 5-slice SMS brain dataset and 6 hours to reconstruct a 3-slice SMS abdominal dataset on the CPU system. For single-slice references, reconstructions were able to run on a GPU (Tesla V100 SXM2, NVIDIA, Santa Clara, CA), which then took only 8-12 minutes per dataset.

Model-based reconstruction techniques generally offer a flexible choice of temporal binning, that is, even a single radial spoke per k-space frame could be employed for accurate parameter estimation. \(^{23} \) However, a certain amount of temporal binning effectively reduces the computational demand as long as the \( T_1 \) accuracy is not compromised. \(^{4,23} \) Here, the number of binned spokes was chosen such that the temporal bin size does not exceed 85 ms, which is sufficiently low to keep the quantification error below 1% as shown previously. \(^{23} \) More specifically, 15, 6, and 4 spokes per k-space frame were selected for single-slice, simultaneous 3-slice and 5-slice model-based brain reconstructions, respectively. For abdominal studies, 25 and 10 spokes per k-space frame were used for single-slice and simultaneous 3-slice reconstructions.
2.5 | $T_1$ analysis

All quantitative $T_1$ results are reported as mean ± standard deviation (SD). Regions-of-interest (ROIs) were carefully selected to minimize partial volume errors using the array-Show tool in MATLAB (MathWorks, Natick, MA). For further analysis, relative difference maps 
\[
\frac{|T_{1\text{est}} - T_{1\text{ref}}|}{T_{1\text{ref}}} \times 100\%
\]
and normalized relative errors 
\[
\frac{\|T_{1\text{est}} - T_{1\text{ref}}\|_2}{\|T_{1\text{ref}}\|_2}
\]
were calculated, respectively, with $T_{1\text{ref}}$ the reference $T_1$ map estimated from a single-slice acquisition and $T_{1\text{est}}$ the $T_1$ map reconstructed from the corresponding multi-slice acquisition. Moreover, the repeatability error between scans was calculated using 
\[
\sqrt{\frac{\sum_{i=1}^{n_s} T_{1\text{diff}}(i)^2}{n_s}},
\]
with $T_{1\text{diff}}(i)$ the $T_1$ difference between different measurements and $n_s$ the number of subjects. In addition, synthetic images are computed for all inversion times and this image series is then converted into a movie showing the recovery of the longitudinal magnetization after the inversion.

3 | RESULTS

The proposed method was first validated in a phantom study using the SMS golden-angle acquisition and the developed SMS model–based reconstruction. Figure 2A shows $T_1$ maps of 3 slices reconstructed with the proposed method together with an IR spin-echo reference and the $T_1$ maps estimated from single-slice IR radial acquisition of the center slice. Visual inspection reveals that the proposed method can completely disentangle the superposed slices and all multi-slice $T_1$ maps are in good agreement with the references. These findings are confirmed by the $T_1$ values of the ROIs in the center slice in Figure 2B, where preservation of good precision (low standard deviation) of the SMS $T_1$ mapping method is also observed. Quantitative results for $T_1$ maps from the other 2 slices are shown in the Supporting Information Table S1, which confirms good $T_1$ accuracy and precision of these 2 slices as well.

Figure 3 demonstrates the effect of the minimum regularization parameter $\alpha_{\text{min}}$ used in the SMS model–based reconstruction.
reconstruction with a multi-slice factor of 5. Low values of $\alpha_{\text{min}}$ result in increased noise in the $T_1$ maps, while high values lead to blurring. A similar effect can be seen in the synthesized image series presented in the Supporting Information Video S1. A value of $\alpha_{\text{min}} = 0.001$ was chosen to balance noise reduction and preservation of image details. This value was used for all multi-slice brain reconstructions. Similarly, $\alpha_{\text{min}} = 0.00025$ was used for all multi-slice abdominal reconstructions.

Figure 4A compares the center-slice $T_1$ maps of a human brain for different multi-slice acquisitions and using model-based reconstruction for a multi-slice factor of 3. Both SMS methods produce $T_1$ maps with less noise than the conventional spoke-interleaved multi-slice method. Furthermore, the SMS $T_1$ values are closer to the single-slice reference, as seen in the relative difference maps as well as the normalized errors. In line with the 3-slice results, Figure 4B shows for a multi-slice factor of 5 that both SMS $T_1$ maps have better SNR and are closer to the reference than the conventional multi-slice method. For both acceleration factors, the SMS golden-angle method further helps to reduce streaking artifacts on the $T_1$ maps. The ROI-analyzed quantitative liver $T_1$ values in Figure 6B confirm good accuracy of all multi-slice methods in comparison to the single-slice $T_1$ map with a best quantitative precision achieved by the SMS golden-angle method.

Figure 7A depicts all $T_1$ maps estimated from a 5-slice SMS golden-angle acquisition as well as the corresponding single-slice $T_1$ maps. All 5-slice $T_1$ maps are visually in good agreement with the corresponding single-slice maps. This is also observed for the other 5 subjects as shown in the Supporting Information Figure S1, indicating that the combination of the SMS golden-angle acquisition with SMS model-based reconstructions can be used to simultaneously acquire $T_1$ maps for 5 slices of a human brain in good quality within 4 seconds. A similar comparison is presented for simultaneous 3-slice abdominal $T_1$ mapping in Figure 7B and Supporting Information Figure S2. In this case, the simultaneous 3-slice datasets were acquired within a single 4-second breathhold. Again, good agreement is reached between the simultaneous 3-slice abdominal $T_1$ maps and the single-slice maps. These results suggest an acceleration factor of 3 can be used for abdominal $T_1$ mapping with the proposed method. Images for all inversion times were

![Figure 3](image_url)
FIGURE 4  A, (Top) Center-slice of 3-slice brain $T_1$ maps from different multi-slice acquisitions using model-based reconstructions with (middle) magnified $T_1$ regions and (bottom) their relative difference maps ($\times 5$) to the single-slice reference $T_1$ map. B, Similar comparisons at a multi-slice factor of 5. Normalized errors are presented at the bottom left on all relative-difference $T_1$ maps.
FIGURE 5  Quantitative $T_1$ values (mean and standard deviation) within ROIs that were manually drawn into the frontal white matter (WM), occipital WM, frontal gray matter (GM) and occipital GM of all $T_1$ maps in Figure 4.

FIGURE 6  A, (Top) Center-slice of 3-slice abdominal $T_1$ maps from different multi-slice acquisitions using model-based reconstructions with (bottom) magnified $T_1$ regions. B, Quantitative $T_1$ values (mean and standard deviation) within ROIs that were manually drawn into the liver region as indicated in A.

WANG ET AL. synthesized for the 5-slice brain and 3-slice liver studies and are presented in the Supporting Information Videos S2 and S3, respectively.

Figures 8 and 9 show $T_1$ values of all 6 subjects for the 2 repetitive scans in both SMS brain and liver studies. The small $T_1$ difference between the repetitive scans demonstrates...
good intrasubject repeatability of the proposed method. The repeatability errors are: frontal white matter: 13 ms (1.8% of the mean), occipital white matter: 4 ms (0.5% of the mean), frontal gray matter: 15 ms (1.1% of the mean), occipital gray matter: 18 ms (1.3% of the mean), and liver: 4 ms (0.5% of the mean). Figure 9 additionally confirms good quantitative agreement between single-slice and SMS liver T1 values for all subjects.

Figure 10 illustrates the use of the proposed SMS T1 mapping technique for the acquisition of a whole-brain T1 map consisting of 25 contiguous slices with a resolution of 0.75 × 0.75 × 5mm3. These datasets were acquired using 5 consecutive 5-slice SMS acquisitions with each having slice distance of 25 mm. As a sufficient delay is necessary between the non-selective inversions, the total acquisition took around 1 minute: Four seconds for each 5-slice SMS acquisition with a waiting period of 10 seconds in between to ensure full recovery of the magnetization.

4 | DISCUSSION

This work describes a fast multi-slice T1 mapping technique which combines simultaneous multi-slice excitations and single-shot IR radial FLASH with an extended nonlinear model-based reconstruction. The present method avoids any coil-calibration steps for SMS reconstruction and uses sparsity constraints to improve precision. Validation studies on a phantom and in 6 healthy subjects show that the combination of SMS golden-angle acquisition and the developed SMS model-based reconstruction technique can obtain high-resolution simultaneous 5-slice brain T1 maps and simultaneous 3-slice abdominal T1 maps with good accuracy, precision, and repeatability within a single inversion recovery of 4 seconds.

In comparison, to reconstruct a fully-sampled image at each time point while still keeping bin size small, the conventional IR Look-Locker technique needs to employ multiple...
**Figure 8** Quantitative brain $T_1$ values (s) in the 4 ROIs of the center slice when using the 5-slice SMS $T_1$ methods for all 6 subjects and 2 repetitive scans. FWM, frontal white matter; OWM, occipital white matter; FGM, frontal gray matter, and OGM, occipital gray matter.

**Figure 9** Quantitative liver $T_1$ values (s) of the center slice when using the 3-slice SMS $T_1$ methods for all 6 subjects and 2 repetitive scans. Note that dashed black lines represent the corresponding liver $T_1$ values from single-slice acquisitions.
inversions and acquire complementary k-space data in each inversion to fulfill the Nyquist criterion. With a bin size of 20 radial spokes (single-slice) and a 256 × 256 matrix, at least $20 \approx (256 \times \pi/2)/20$ inversions are needed. Thus, the undersampling factor is 20 for model-based reconstruction in the single-shot single-slice method. With the extension to SMS described in the present work, the acceleration factor is further enhanced by an additional factor of 3-5. The present method achieves 0.8-1.33 seconds per $T_1$ map within a single inversion recovery and 2.8-4.67 seconds per map when taking into account a 10-second delay in a multi-slice protocol with several inversions. This compares well to other recent radial $T_1$ mapping approaches with IR Look-Locker based acquisitions recently described in the literature.$^{26,32}$

In contrast to many other quantitative SMS MRI techniques,$^{28,34,35}$ the proposed method integrates coil-sensitivity estimation into the model-based reconstruction framework, avoiding additional calibration scans, which further reduces miscalibration errors in case of motion, especially when imaging moving organs such as abdomen or heart. Moreover, the proposed method dispenses with intermediate image reconstruction, enabling the reconstruction of high-quality $T_1$ maps directly from k-space which does not require binning. This property is especially beneficial for $T_1$ mapping of multiple slices at higher acceleration factors where other methods need to trade off image quality against accuracy when choosing the bin size.$^{36,50}$ The spoke-interleaved results in this study are noisier than the ones presented in ref. 31. The main
reason might be that measurements in the previous work\textsuperscript{31} were done on a different scanner using a 64-channel head coil while this study employed a 20-channel head coil. Different parameter choices for sequence and reconstruction may also be a contributing factor. In this study, we used identical parameters as used in the proposed SMS model–based method to make a direct comparison possible.

In the present work, we use a radial FLASH readout while other studies employ EPI or 3D spiral to achieve high-resolution brain mapping.\textsuperscript{51,52} While radial FLASH is less efficient in covering k-space, with short echo times it is much less sensitive to off-resonance effects than spiral or EPI trajectories and is not affected by geometric distortions. Due to the intrinsic oversampling of the k-space center, radial FLASH is also more robust to motion, which will be beneficial in abdominal and cardiac applications. An alternative to multi-slice T\textsubscript{1} mapping is 3D imaging using a radial stack-of-stars sequence or other 3D sequences.\textsuperscript{52} 3D sequences should provide even better SNR than 2D SMS imaging and allow for isotropic T\textsubscript{1} mapping.\textsuperscript{26,52} The proposed model-based reconstruction method is also applicable to 3D T\textsubscript{1} mapping. However, 3D sequences need to employ multi-shot acquisitions, in which case data over the duration of a complete scan (usually in the order of minutes) have to be combined for parameter estimation. This makes 3D imaging much more sensitive to motion than their 2D SMS counterparts.\textsuperscript{34}

For radial sampling, the use of a golden angle in the partition dimension has been shown to have better performance than the use of aligned spokes for undersampled stack-of-stars 3D volume MRI\textsuperscript{37} and 2D radial SMS parallel imaging using NLINV.\textsuperscript{38} In this work, we have adopted the same strategy for SMS model–based parameter mapping. Our results confirm a slightly better performance of this golden-angle strategy over the aligned case. Combination of such a sampling strategy and model-based reconstructions may be further exploited for single-shot SMS myocardial T\textsubscript{1} mapping, where part of the IR data (eg, systolic data) would be discarded prior to model-based T\textsubscript{1} estimations.\textsuperscript{53} The proposed method is also applicable to whole-liver imaging where we need to perform the single-shot acquisition multiple times, that is, with multiple breathholds to achieve the desired volume coverage. As the delay time can be as short as 3 seconds for liver studies,\textsuperscript{34} covering the entire liver with 30 slices using ten 4-second breathhold SMS-3 acquisitions interrupted by nine 3-second time gaps when the subject is allowed to breath freely required a minimum acquisition time of 67 seconds. With a longer delays of 10 seconds between breathholds for more patient convenience this scan could still be performed in 2 minutes.

The non-selective inversion pulse used in this study is not optimal for whole-brain T\textsubscript{1} mapping as it necessitates a delay time between successive SMS acquisitions. The 10-second delay time we employed is very high as usually 3-4 seconds should be enough for brain applications.\textsuperscript{26} Furthermore, it has been reported\textsuperscript{30,32} that there is little difference in T\textsubscript{1} accuracy between non-selective and slab-selective inversion pulses for brain T\textsubscript{1} mapping. With adapted excitation pulses and acquisition strategies, we expect to eliminate most of the delay time when combining a slab-selective inversion with the proposed simultaneous multi-slice T\textsubscript{1} mapping technique for full brain applications in future studies.

The other limitation of the proposed method is the long computation time, especially for model-based reconstruction of the SMS golden-angle datasets: All the data from multiple slices have to be held in memory simultaneously during iterations, which still prevents the use of GPUs. In principle, the alternative methods such as subspace methods have to deal with the same amount of data, but recent implementations use smart computational strategies to reduce the amount of memory and can then achieve very fast reconstruction.\textsuperscript{12,42,55} The key difference between subspace and the nonlinear methods is that the latter does not need any approximations for the signal models, that is, a minimal number of physical parameters could describe the desired MR signal precisely. In contrast, subspace methods have to approximate the MR signal using a few principal coefficients, which then leads to compromised accuracy or precision. While computation times reported in this work for the proposed model-based reconstruction on CPUs are still very high, newer generations of GPUs with larger memory will enable much faster reconstructions. Preliminary results obtained by using a smaller matrix size are very encouraging: When reducing the in-plane resolution from 0.75 ×0.75 mm\textsuperscript{2} (matrix size: 512 × 512) to 1.0 × 1.0 mm\textsuperscript{2} (matrix size: 384 × 384), the SMS 5-slice model-based reconstructions could already run on a GPU, which then took only around 14 min per dataset. Similarly, the 1.0 ×1.0 mm\textsuperscript{2} SMS 3-slice reconstruction took around 8 min per dataset.

\section{Conclusion}

The proposed combination of simultaneous multi-slice excitations, single-shot IR radial FLASH, and calibrationless model-based reconstruction allows for efficient high-resolution multi-slice T\textsubscript{1} mapping with good accuracy, precision, and repeatability.

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DATA AVAILABILITY STATEMENT
In the spirit of reproducible research, code to reproduce the experiments is available on https://github.com/mriereon/sms-T1-mapping. The raw k-space data used in this study can be downloaded from https://doi.org/10.5281/zenodo.3969809.

ORCID
Xiaqing Wang https://orcid.org/0000-0001-7036-7930
Sebastian Rosenzweig https://orcid.org/0000-0001-7972-2134
Nick Scholand https://orcid.org/0000-0002-8876-0236
H. Christian M. Holme https://orcid.org/0000-0002-8619-0444
Martin Uecker https://orcid.org/0000-0002-8850-809X

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Supporting Information

Additional Supporting Information may be found online in the Supporting Information section.

**FIGURE S1** $T_1$ maps for 5 simultaneously acquired slices of the human brain and the corresponding single-slice $T_1$ maps for 5 subjects

**FIGURE S2** $T_1$ maps for 3 simultaneously acquired abdominal slices and the corresponding single-slice $T_1$ maps for 5 subjects

**TABLE S1** $T_1$ relaxation times (ms, mean ± SD) for the experimental phantom in Figure 2

**VIDEO S1** Synthesized image series representing recovery of the longitudinal magnetization after inversion for the 5-slice SMS brain study (center-slice) using model-based reconstruction with different minimum regularization parameters, that is, $\alpha_{\text{min}} = 0.0005, 0.001, 0.0015, 0.002$, from left to right, respectively

**VIDEO S2** Synthesized image series representing recovery of the longitudinal magnetization after inversion for 5 simultaneously acquired slices of a human brain when using a bin size of 82 ms. The acquisition time for all 5 slices is 4 seconds

**VIDEO S3** Synthesized image series representing recovery of the longitudinal magnetization after inversion for 3 simultaneously acquired slices of a human liver using a bin size of 81 ms. The acquisition time for all 3 slices is 4 seconds

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