NUMERICAL SIMULATIONS OF IMPULSIVELY GENERATED ALFVÉN WAVES IN SOLAR MAGNETIC ARCADES

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ABSTRACT

We perform numerical simulations of impulsively generated Alfvén waves in an isolated solar arcade, which is gravitationally stratified and magnetically confined. We study numerically the propagation of Alfvén waves along the magnetic structure that extends from the lower chromosphere, where the waves are generated, to the solar corona, and analyze the influence of the arcade size and the width of the initial pulses on the wave propagation and reflection. Our model of the solar atmosphere is constructed by adopting the temperature distribution based on the semi-empirical VAL-C model and specifying the curved magnetic field lines that constitute the asymmetric magnetic arcade. The propagation and reflection of Alfvén waves in this arcade is described by 2.5-dimensional magnetohydrodynamic equations that are numerically solved by the FLASH code. Our numerical simulations reveal that the Alfvén wave amplitude decreases as a result of a partial reflection of Alfvén waves in the solar transition region, and that the waves which are not reflected leak through the transition region and reach the solar corona. We also find that the decrement of the attenuation time of Alfvén waves for wider initial pulses. Moreover, our results show that the propagation of Alfvén waves in the arcade is affected by the spatial dependence of the Alfvén speed, which leads to phase mixing that is stronger for more curved and larger magnetic arcades. We discuss the processes that affect the Alfvén wave propagation in an asymmetric solar arcade and conclude that besides phase mixing in the magnetic field configuration, the plasma properties of the arcade, the size of the initial pulse, and the structure of the solar transition region all play a vital role in the Alfvén wave propagation.

Key words: magnetohydrodynamics (MHD) – Sun: atmosphere – Sun: corona – Sun: magnetic fields

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1. INTRODUCTION

Arcades are gravitationally stratified and magnetically confined structures in the solar atmosphere. Their physical properties are determined by flows of plasma along these arcades and the heating resulting from energy dissipation by different waves (Cadez et al., 1994; Innes et al., 2003; McKenzie & Savage, 2009). Investigations of the magnetic topology of such arcades (Biskamp & Welter, 1989; Mikić et al., 1989) and magnetohydrodynamic (MHD) wave propagation in these structures (e.g., Del Zanna et al., 2005; Selwa et al., 2005, 2006; Díaz et al., 2006) are potential areas of research that reveal both wave heating and plasma dynamics. In more recent studies carried out by Gruszczki & Nakariakov (2011), the excitation of slow magnetoacoustic waves was investigated in a system of magnetic arcades. Specifically, the antisymmetric kink mode of magnetoacoustic waves was modeled in the magnetic arcades and used for determination of the arcade magnetic field, which is often referred to as MHD seismology.

Theoretical predictions resulting from the above studies have been supplemented by several significant efforts to observe such waves in the magnetic arcades. Verwichte et al. (2004) detected damped standing kink oscillations in the arcades using the Transition Region and Coronal Explorer (TRACE) observations. Verwichte et al. (2010) reported on transverse kink oscillations in the coronal arcades observed by SOHO/EIT and STEREO, and used the results to invoke the spatial MHD seismology of these magnetic structures to estimate their local plasma conditions.

Previous studies of magnetoacoustic waves were also supplemented by investigations of the propagation of purely incompressible transverse (Alfvén) waves in such magnetic arcades in the solar atmosphere. Since the magnetic field serves as a guide for Alfvén waves, it is worthwhile to study these waves in magnetic field structures like arcades. Arregui et al. (2004) studied MHD waves, including Alfvén, coupled Alfvén and fast magnetoacoustic (fast, henceforth) waves, and the magnetic arcade oscillations connected with the propagation of these waves. In a cold plasma approximation, they showed that the linear coupling of discrete fast modes, which are characterized by a discrete spectrum of frequencies and a global velocity structure, and Alfvén continuum modes, which are characterized by a continuous spectrum of frequencies and a velocity perturbation confined to given magnetic surfaces, leads to modes with mixed properties that arise in the magnetic arcades.

Similarly, Oliver et al. (1996) also investigated the mixed fast magnetoacoustic and Alfvén waves in the form of MHD perturbations excited in the magnetic arcades. Due to resonant coupling, Rial et al. (2010) found that the fast wave transfers its energy to the Alfvénic oscillations localized around a particular magnetic surface within the arcade, thus producing the attenuation of the initial fast MHD mode. Moreover, they discussed another case in which the generated fast wavefront leaves its energy on several magnetic surfaces within the arcade. The system is therefore able to trap energy in the form of Alfvénic oscillations, which are subsequently phase mixed to smaller spatial scales.
Gruszecki et al. (2007) considered the energy loss by Alfvén waves for straight and curved magnetic fields, and found a relation between the energy loss and the amplitude of the initial wave pulse. Results clearly showed that Alfvén waves in a magnetic arcade experience a decrease of their amplitude and that this decrease is caused by partial reflection of the waves from the solar transition region (Gruszecki et al. 2007). The partial reflection of Alfvén waves results from a steep gradient of the Alfvén speed in the transition region due to a significant density drop in this region of the solar atmosphere.

An important problem for Alfvén wave chromospheric leakage in coronal loops was studied by Ofman (2002) in a normalized visco-resistive nonlinear 1.5-dimensional MHD model, for which the Alfvén leakage time was computed. Moreover, Ofman & Wang (2007) constructed an MHD model that allowed them to examine the periodic oscillations in their coronal loop and compare the results to those observed by the Solar Optical Telescope on board Hinode.

Del Zanna et al. (2005) performed numerical studies of Alfvén waves triggered by solar flare events in an isothermal and symmetric arcade model, and showed that these waves propagate back and forth along the arcade and quickly decay. According to the authors, the fast decay of these waves explains the observed damping of the amplitudes of the oscillations, and the efficiency of Alfvén wave decay is related to the stratification of the solar atmosphere as well as to a gradient of the magnetic field along the arcade. Miyagoshi et al. (2004) investigated oscillations of a symmetric solar arcade and showed that the amplitude of the loop oscillations decreases exponentially in time due to the energy transport by fast-mode MHD waves.

Based on the above results, we may conclude that curved magnetic fields, such as those existing in the solar magnetic arcades, effectively increase the wave energy leakage. Moreover, the stronger the Alfvén wave pulse amplitudes are the more efficient the generation of fast magnetoacoustic waves will be. Nevertheless, additional studies, in which the solar atmosphere model is extended to include the solar chromosphere and transition region and a broader range of physical parameters for an asymmetric magnetic field configuration is considered, are urgently needed. Therefore, the main goal of this paper is to perform such studies and significantly extend the previous work of Del Zanna et al. (2005) and Miyagoshi et al. (2004).

In our approach, we consider an asymmetric, stratified, and non-isothermal solar arcade, we assume that the temperature profile along the arcade is based on the VAL-C semi-empirical model of the solar atmosphere (Vernazza et al. 1981), and we follow Low (1985) in constructing a magnetic field model of the arcade. An important difference between our approach and that presented by Del Zanna et al. and Miyagoshi et al. is that we impulsively generate Alfvén waves by launching them in the solar chromosphere, just above the solar photosphere, whereas in Del Zanna’s work the waves are triggered by the onset of a solar flare in the solar corona. Since flares are highly episodic events, we impulsively generate Alfvén waves by launching them in the solar transition region and a broader range of physical parameters for asymmetric magnetic fields, such as those existing in the solar magnetic arcades, effectively increase the wave energy leakage. Moreover, the stronger the Alfvén wave pulse amplitudes are the more efficient the generation of fast magnetoacoustic waves will be. Nevertheless, additional studies, in which the solar atmosphere model is extended to include the solar chromosphere and transition region and a broader range of physical parameters for an asymmetric magnetic field configuration is considered, are urgently needed. Therefore, the main goal of this paper is to perform such studies and significantly extend the previous work of Del Zanna et al. (2005) and Miyagoshi et al. (2004).

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2. NUMERICAL MODEL OF ALFVÉN WAVES

2.1. MHD Equations

We consider a gravitationally stratified and magnetically confined plasma in a structure that resembles an arcade, which is described by the following set of ideal MHD equations:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0,$$

$$\rho \frac{\partial \mathbf{V}}{\partial t} + \rho (\mathbf{V} \cdot \nabla) \mathbf{V} = -\nabla p + \frac{1}{\mu} (\nabla \times \mathbf{B}) \times \mathbf{B} + \rho \mathbf{g},$$

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{V} \times \mathbf{B}),$$

$$\nabla \cdot \mathbf{B} = 0,$$

$$\frac{\partial p}{\partial t} + \mathbf{V} \cdot \nabla p = -\gamma p \nabla \cdot \mathbf{V} + \frac{k_B}{m} \rho T,$$

where $\rho$ is the mass density; $p$ is the gas pressure; and $\mathbf{V}$, $\mathbf{B}$, and $\mathbf{g}$ (0, $-g$, 0) represent the plasma velocity, the magnetic field, and the gravitational acceleration, respectively. In addition, $T$ is temperature, $m$ is particle mass, which was specified by a mean molecular weight value of 2.4 (O. Steiner, private communication), $k_B$ is Boltzmann’s constant, $\gamma = 5/3$ is the adiabatic index, and $\mu$ is the magnetic permeability of the plasma. The value of $g$ is equal to 274 m s$^{-2}$.

Note that Del Zanna et al. (2005) worked under the assumption of isothermal plasma, $\gamma = 1$, which resulted in the elimination of the energy equation, and thermal pressure was described by the ideal gas law of Equation (6). This approximation greatly simplifies numerical methods, particularly in regions of strongly magnetized plasma where negative gas pressure can set in.

2.2. A Model of the Static Solar Atmosphere

We consider a model of the static ($\partial/\partial t = 0$) solar atmosphere with an invariant coordinate $z$ ($\partial/\partial z = 0$), but allow the
The components of the velocity \( V_z \) and magnetic field \( B_z \) to vary with \( x \) and \( y \). In such a 2.5-dimensional (2.5D) model, the solar atmosphere is in static equilibrium \( (\nabla \cdot V = 0) \) with the force-free and current-free magnetic field defined by

\[
(\nabla \times B_x) \times B_z = 0, \quad \nabla \times B_z = 0.
\]  

(7)

Here, the subscript \( e \) corresponds to equilibrium quantities. We adopt a realistic plasma temperature profile given by Low (1985), in which

\[
B_e(x, y) = \nabla \times (A\hat{z})
\]  

(8)

is an equilibrium magnetic field with \( \hat{z} \) being a unit vector along the \( z \) direction and \( A \) denoting the magnetic flux function given by

\[
A(x, y) = \frac{x(y_{\text{ref}} - b)^2}{(y - b)^2 - x^2} B_{\text{ref}}.
\]  

(9)

Here, \( b \) is a constant, which we choose and set equal to \( b = -5 \) Mm, and \( B_{\text{ref}} \) is the magnetic field at the reference level \( y_{\text{ref}} = 10 \) Mm.

Vectors of the magnetic field, resulting from Equation (8), are displayed in Figure 1. The magnetic field is defined by the magnetic pole which is located at the point \( (x = 0 \text{ Mm}, y = -5 \text{ Mm}) \). Note that at a given altitude \( y \), the magnetic field is strongest around the line \( x = 0 \) Mm where it is essentially vertical. However, further out, the magnetic field declines with larger values of \( |x| \), revealing its curved structure. Such a magnetic field corresponds to an isolated asymmetric magnetic arcade.

As a result of Equations (2) and (7), the pressure gradient is balanced by the force of gravity:

\[
-\nabla p_e + \varrho_e g = 0.
\]  

(10)

Using the ideal gas law given by Equation (6) and the \( y \) component of the hydrostatic pressure balance described by Equation (10), we express the equilibrium gas pressure and mass density as

\[
p_e(y) = \rho_{\text{ref}} \exp \left( -\int_{y}^{y_{\text{ref}}} \frac{dy}{\Lambda(y)} \right),
\]  

(11)

\[
\varrho_e(y) = \frac{p_e(y)}{g\Lambda(y)},
\]  

(12)

where

\[
\Lambda(y) = \frac{k_B T_e(y)}{mg}
\]  

(13)

is the pressure scale-height, and \( \rho_{\text{ref}} \) denotes the gas pressure at the reference level.

We adopt a realistic plasma temperature profile given by the semi-empirical VAL-C model (Vernazza et al. 1981) that is extrapolated into the solar corona (Figure 2, top panel). In our model, the temperature attains a value of about \( 5 \times 10^3 \text{ K} \) at \( y = 1.5 \text{ Mm} \) and increases to about \( 1.5 \times 10^6 \text{ K} \) in the solar corona at \( y = 10 \text{ Mm} \). Higher up in the solar corona, the temperature is assumed to be constant. The temperature profile uniquely determines the equilibrium mass density and gas pressure profiles. At the transition region, which is located at \( y \approx 2.7 \text{ Mm}, T_e \text{ exhibits an abrupt jump (Figure 2, top panel), but } \varrho_e(y) \text{ and } p_e(y) \text{ experience a sudden drop off with atmospheric height (not shown).}

In this model, the Alfvén speed, \( c_A \), varies in both the \( x \) and \( y \) directions and it is expressed as follows:

\[
c_A(x, y) = \frac{|B_x(x, y)|}{\sqrt{\mu \varrho_e(y)}}.
\]  

(14)

Its profile is displayed in Figure 2 (bottom panel). Note that the Alfvén speed is non-isotropic; higher values are located near \( x_0 = 0 \text{ Mm} \) where the magnetic field is stronger, while \( c_A \) decreases with larger values of \( x_0 \). In the chromosphere, \( c_A(x = 0 \text{ Mm}, y = 1.75 \text{ Mm}) \) is about \( 25 \text{ km s}^{-1} \). The Alfvén speed rises abruptly through the solar transition region, reaching a value of \( c_A(x = 0 \text{ Mm}, y = 10 \text{ Mm}) = 10^3 \text{ km s}^{-1} \) (Figure 2, bottom panel). The increase of \( c_A(x = 0 \text{ Mm}, y) \) with height results from a faster decrease of \( \varrho_e(y) \) than \( B_x(x = 0 \text{ Mm}, y) \) with atmospheric height.
3. NUMERICAL SIMULATIONS OF MHD EQUATIONS

To solve Equations (1)–(6) numerically, we use the FLASH code (Fryxell et al. 2000; Lee & Deane 2009; Lee 2013), in which a third-order unsplit Godunov-type solver with various slope limiters and Riemann solvers as well as adaptive mesh refinement (MacNeice et al. 1999) are implemented. The minmod slope limiter and the Roe Riemann solver (e.g., Toth 2000) are used. We set the simulation box as (1 Mm, 28.5 Mm) \times (1 Mm, 11 Mm) and impose boundary conditions fixed in time for all plasma quantities in the x and y directions, while all of the plasma quantities remain invariant along the z direction; however, note that both \( \mathbf{v} \) and \( \mathbf{B} \) differ from zero.

In our present work, we use a static, non-uniform grid with a minimum (maximum) level of refinement set to 4 (6). We performed grid convergence studies by refining this by a factor of two. As the numerical results remained essentially similar for the grid of maximum blocks levels 6 and 7, we adopted the former to obtain the results presented in this paper. Note that the small size blocks of the numerical grid occupy the solar transition region and the region located along the Alfvén wave front to obtain the results presented in this paper. Note that in our 2.5D model, the Alfvén waves decouple from the magnetoacoustic waves and it can be described solely by \( V_z(x, y, t) \). As a result, the initial pulse triggers Alfvén waves which in the linear limit are approximately described by the following wave equation:

\[
\frac{\partial^2 V_z}{\partial t^2} = c^2_{A}(x, y) \frac{\partial^2 V_z}{\partial s^2},
\]

where s is the coordinate along a magnetic field line.

4. RESULTS OF NUMERICAL SIMULATIONS

We simulate small amplitude and impulsively excited Alfvén waves and investigate their propagation along magnetic field lines which are parallel to the magnetic vectors shown in Figure 1. This magnetic field configuration mimics an asymmetric solar arcade, which is more realistic than that considered by Del Zanna et al. (2005).

4.1. Initial Stage of Wave Propagation

The Gaussian pulse of the initial perturbation in the z component of the velocity, described by Equation (15), decouples into two pulses moving in opposite directions. The downwardly propagating pulse fades very fast; however, the second pulse propagates through the chromosphere and transition region to the solar corona (Figure 4).

As a result of several effects, such as the finite size of the Alfvén wave pulse, inclination of the magnetic field, and highly inhomogeneous Alfvén speed, \( c_{A}(x, y) \), the wave signal in our numerical simulations is deformed and elongated while in the arcade passing through the transition region. First, the initially circular wave profile is distorted to ellipsoidal shape because the Alfvén speed slightly increases along the inclined magnetic field lines (Figure 5), and then becomes significantly elongated above the transition region (Figure 4(c)) due to a sudden increase of the Alfvén speed (Figure 5).

This clearly shows that the upper part of the wave signal, propagating along the magnetic field lines, penetrates the solar corona earlier than the middle and bottom parts of the signal (Figure 4(b)). Moreover, the upper part of the wave follows along a different (upper) magnetic field line than the right part of the wave which propagates over the lower magnetic field line, which results in the deformation of the initial pulse and finally intensifies the phase mixing that can be seen in

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\]

where s is the coordinate along a magnetic field line.
Figure 4. Spatial profiles of the velocity $V_z(x, y, t)$ near the point of initial perturbation for the case of $x_0 = 2\,\text{Mm}$, $w_x = 0.1\,\text{Mm}$ at $t = 5\,\text{s}$, $t = 8\,\text{s}$, $t = 11\,\text{s}$, $t = 14\,\text{s}$, $t = 18\,\text{s}$, and $t = 21\,\text{s}$, presenting propagation through the transition region and the evolution of the initial pulse. A movie of the above figure is available at www.article.com, Fig4.avi.

(A color version of this figure is available in the online journal.)

panels (d) and (e) of Figure 4. Here, the upper part of the wave signal located in the upper magnetic field lines, illustrated as a white patch (Figures 4(d) and (e)), is in a different phase than the signal located in the lower magnetic field line, which already passed the transition region. This additional process of wave deformation at the transition region significantly influences Alfvén wave propagation in the curved coronal arcades, introducing different phases of the wave signal in the arcade at the beginning stage. Note that the Alfvén waves suffer from partial reflection from the transition region and a small signal propagates backward into the solar surface, which can be spotted at $(x, y) \approx (2\,\text{Mm}, 1.8\,\text{Mm})$ in Figures 4(e) and (f).

4.2. Different Spatial Positions of Initial Pulses

In our approach for a fixed value of $y_0$, the length and curvature of the magnetic field lines vary with $x_0$. For a smaller value of $x_0$, a magnetic line is longer, more curved, and less inclined to the horizontal direction (Figure 1); also, Alfvén speed $c_A(x, y)$ experiences a larger structuring there (Figure 2, bottom panel). Meanwhile, a larger value of $x_0$ corresponds to a shorter, less curved, and more inclined magnetic field lines as well as less varying $c_A(x, y)$. Here, we consider two different cases of initial pulse position: $x_0 = 2\,\text{Mm}$ and $x_0 = 3\,\text{Mm}$. In the first case, the Alfvén waves propagate higher up along longer and more curved magnetic field lines. However, in the case of $x_0 = 3\,\text{Mm}$, the inclination of the magnetic field lines to the $x$ axis is much larger and this results in approximately two times smaller size of the arcade with less curved field lines. In Figure 5, we note that $c_A(s)$ varies less along the magnetic field line, $s$, for a small arcade, reaching a value of $2\,\text{Mm}\,\text{s}^{-1}$ (dashed line), while for a large arcade it attains $2.4\,\text{Mm}\,\text{s}^{-1}$ (solid line). Here, a value of $s = 0$ corresponds to the point at which the initial perturbation was launched, $(x_0, y_0)$, equal to $(2\,\text{Mm}, 1.75\,\text{Mm})$ for the large arcade (solid line) and $(3\,\text{Mm}, 1.75\,\text{Mm})$ for the small arcade (dashed line).

4.2.1. Large Arcade

Our numerical results are presented in Figure 6, which illustrates the spatial profiles of Alfvén waves generated by the initial Gaussian pulse given by Equation (15). This pulse triggers counter-propagating Alfvén waves (e.g., Murawski & Musielak 2010). The wave that propagates downward enters
a region of small Alfvén speed, which results from high mass density there. The presented results show that the evolution of the downwardly propagating waves (Figure 4) is much less dynamic than the evolution of the Alfvén waves that already reach the upper regions of the solar atmosphere.

The upwardly propagating Alfvén waves, reaching the transition region, accelerate due to an increase of the local Alfvén speed (Figure 2, bottom panel, and Figure 5, solid line) and penetrate into the solar corona. In Figure 6(a), the wave signal arrived at a level of $y = 9$ Mm. At $t = 26$ s (panel (b)), the Alfvén waves are at the apex while fanning its spatial profile as a result of diverging magnetic field lines (Figure 1) and the spatial variation of the Alfvén speed (Figure 2, bottom panel). This process becomes even more pronounced in time as the Alfvén waves penetrate the regions of more diverged field lines. Behind the Alfvén wave signal, there is visible fanning of a negative value of $V_z$ (violet-white patch) which remains after the Alfvén wave passes through the plasma medium (Murawski & Musielak 2010).

Now, the violet patch seen in Figure 6 becomes elongated and contains a white subregion located at $x = 12$ Mm, $y = 7$ Mm (panel (b)). This white subregion corresponds to negative ($V_z \approx -2.1$ km s$^{-1}$) values of the transversal velocity while the nearby positive velocity ($V_z \approx 6.4$ km s$^{-1}$) region is represented by a red patch. This results from the finite-size of the initial pulse whose left and right sides have to pass significantly different distances, because the magnetic field line along the left side path is longer than the magnetic field line along the right side in the considered arcade. Moreover, a strong fanning of the wave signal spatial profile is a consequence of the Alfvén speed, $c_A(x, y)$, which attains different values along different magnetic interfaces (Figure 2, bottom panel). At $t = 36$ s, the already downwardly propagating Alfvén waves reach the transition region (panel (c)) and they undergo partial reflection from this region.

The resulting wave reflection can be well seen in consecutive moments of time, e.g., at $t = 46$ s (panel (d)) and at $t = 56$ s (panel (e)), respectively. However, at later times, the Alfvén wave profiles become more complicated; we note a partial reflection of the wave signal with a negative value of $V_z$, illustrated by a narrow elongated violet-white patch (panels (e) and (f)). At $t = 66$ s, the Alfvén waves reflect again at the left side, near $x_0 = 2$ Mm, and propagate with positive phase velocity (red patch) at $t = 76$ s with an amplitude of $V_z \approx 4.2$ km s$^{-1}$ in the right direction. We observe a long, narrow signal seen as a red patch which reaches the transition region near $x_0 = 21$ Mm at $t = 86$ s (panel (h)). Reflections of the Alfvén waves are well observed at $t = 86$ s (panel (h)) and $t = 96$ s (panel (i)) as violet-white patches near $x_0 = 21$ Mm. Such reflections result in complex Alfvén wave spatial profiles. We provide details on partial reflection in Section 4.4 where we evaluate the corresponding reflection coefficient.

Figure 7 presents in some detail the Alfvén waves reflection. The arriving waves (panel (a), red patch) hit the transition region and begin reflecting there, decreasing its amplitude, which is well observed in consecutive moments of time. In panel (b), the reflected, backwarsly propagating wave is illustrated by a violet-white patch, superimposed on the arriving negative phase waves. The effect of the superimposition of the wave signals is significant, because of the fanning of the wave spatial profiles, which are a consequence of a large arcade where the Alfvén speed gradient and diverged magnetic field lines are large. At later moments of time (panels (e) to (h)), we also see the evolution of the lagging wave signals reflected from the transition region as a red patch under the backward propagating main signal (violet-white patch).

Note that there are clearly observed small partially non-reflected (transmitted) Alfvén waves propagating downward into the solar surface under the transition region. These waves are in phase and their amplitude is about 1 km s$^{-1}$.

It is worth comparing our results to those previously obtained by Del Zanna et al. (2005), who considered an isothermal asymmetric solar arcade with a transverse signal undergoing reflection from the transition region. In our non-isothermal asymmetric arcade, the numerical results show how the Alfvén wave pulse is widened by the diverged magnetic field lines, becomes gradually reflected in the transition region, and creates a non-regular structure of the reflected wave signal (see Figure 6, bottom-right). Later on, the diverged magnetic field configuration, inhomogeneous Alfvén speed, difference of magnetic field lengths, and reflected wave interactions with the ongoing wave train further complicate the spatial velocity profiles in the arcade.

### 4.2.2. Short Arcade

The spatial profiles of Alfvén waves, which result from the initial Gaussian pulse given by Equation (15), with $x_0 = 3$ Mm and $u_x = 0.2$ Mm, are presented in Figure 8. The initial pulse triggers the counter-propagating Alfvén waves in a comparatively less curved magnetic arcade. In this case, the process of initial deformation of the wave pulse during its propagation through the transition region is more effective because the magnetic field lines are more horizontal than in the case of $x_0 = 3$ Mm. The upper part of the signal propagates earlier than the rest of the pulse and strongly influences the phase mixing. On the other hand, a smaller arcade results in less diverged magnetic lines and less $Vc_A(x, y)$, which consequently significantly reduces the fanning process of the wave signal.

Such a smaller arcade causes that a wave signal ranges all arcade region. At $t = 20$ s (panel (b)) and later, the outer edge of the arcade with its large length clearly reveals a phase difference of the transverse wave velocity profiles compared to the same in

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**Figure 5.** Alfvén speed, $c_A$, along the magnetic line, which crosses the point $(x_0, y_0) = (2$ Mm, 1.75 Mm) (solid line) and the point $(x_0, y_0) = (3$ Mm, 1.75 Mm) (dashed line).
Figure 6. Spatial profiles of transverse velocity $V_z(x, y, t)$ for $x_0 = 2$ Mm, $w_x = 0.2$ Mm at $t = 16$ s, $t = 26$ s, $t = 36$ s, $t = 46$ s, $t = 56$ s, $t = 66$ s, $t = 76$ s, $t = 86$ s, $t = 96$ s, and $t = 106$ s (from top left to bottom right). A movie of the above figure is available at www.article.com, Fig6.avi.

(A color version of this figure is available in the online journal.)
the core of the arcade. We observe several wave signal reflections from the transition region in Figure 8. The violet-white patch in panels (d) and (e) represents reflected Alfvén waves that propagate to the left. When they reach the transition region near \( x = 3 \) Mm, they become reflected and propagate again to the right (panels (f) and (g)) to suffer reflection once again near \( x = 16 \) Mm, which is clearly seen at \( t = 44 \) s (panel (h)), and go back into \( x = 3 \) Mm (panels (i) and (j)). It should be noted that the initial pulse width was assumed to be the same as in the case of \( x_0 = 2 \) Mm (Figure 6).
4.2.3. Comparison

In the presented vertical cross-sections of the Alfvén wave profiles, we observe a difference in the wave propagation for large (Figure 9, top panel) and small arcades (Figure 9, bottom panel). The cross-section for the case of $x_0 = 2$ Mm ($x_0 = 3$ Mm) shows the region near the apex of the arcade, $x = 12$ Mm ($x = 9$ Mm), and three moments of time when the wave signal passes the apex: $t = 22$ s ($t = 20$ s), $t = 72$ s ($t = 40$ s), and $t = 124$ s ($t = 60$ s), which are illustrated in the top (bottom) panel of Figure 9 by solid, dashed, and dotted line, respectively. The main difference between these two
cross-sections is the compact shape of the Alfvén wave in the short arcade during all three moments of time compared to the large arcade. This is a result of less diverged magnetic lines, which spread the signal up to a width equal to 5 Mm in the case of $x_0 = 2$ Mm, while in the case of $x_0 = 3$ Mm the pulse width is about 2 Mm.

We also find a difference in the negative phase amplitudes. Already after one period, the Alfvén wave cross-section in the large arcade (Figure 9, top panel) exhibits minima with negative values of $V_z$ accompanying the main wave signal. At $t = 72$ s (dashed line), the first opposite-sign phase with an amplitude of $V_z \simeq -2.2$ km s$^{-1}$ at $y \simeq 8.8$ Mm is a part of the elongated main wave signal still following into the transition region located near $x = 2$ Mm to suffer reflection (Figure 6(g), upper violet white patch), while the second opposite-sign phase with an amplitude of $V_z \simeq -0.8$ km s$^{-1}$ at $y \simeq 6.6$ Mm is a signal that lags behind the main Alfvén signal, which can be well seen in panel (g) of Figure 6 (lower violet patch). At later times, at $t = 124$ s (dotted line), the negative value of $V_z$ has a similar form, however, the amplitudes are $V_z \simeq -1.4$ km s$^{-1}$ at $y \simeq 7.6$ Mm and $V_z \simeq -0.8$ km s$^{-1}$ at $y \simeq 6.7$ Mm.

In the case of a short arcade (Figure 9, bottom panel) for which the divergence of the magnetic lines and the gradient of $c_A$ are smaller, the opposite-sign phases at the cross-section states are only 0.9% of the main wave signal amplitude, equal to $V_z \simeq 5.6$ km s$^{-1}$ at $t = 20$ s (solid line), 7% of the amplitude, equal to $V_z \simeq 3.8$ km s$^{-1}$ at $t = 40$ s (dashed line), and 15.2% of the amplitude, equal to $V_z \simeq 2.5$ km s$^{-1}$ at $t = 60$ s (dotted line).

Figure 10 illustrates the time signatures of $V_z$, collected at points near the apex of each arcade. The time signatures for the cases of $x_0 = 2$ Mm, $x_0 = 2.5$ Mm, and $x_0 = 3$ Mm are presented in the top, middle, and bottom panels, respectively. We set the detection point for the case of $x_0 = 2$ Mm to be at $(x = 12$ Mm, $y = 7$ Mm), for the case of $x_0 = 2.5$ Mm to be at $(x = 11$ Mm, $y = 5.1$ Mm), and for the case of $x_0 = 3$ Mm to be at $(x = 9$ Mm, $y = 4.2$ Mm). Time signatures for smaller arcades ($x_0 = 2.5$ Mm and $x_0 = 2$ Mm) have a regular harmonic shape, but the time signature for the large arcade exhibits action on the fanning process that results in superimposition of incoming and reflected wave signals in $V_z$, and finally in the non-regular shape of $V_z$ oscillations. Note that the amplitude of the Alfvén waves decays with time and that $V_z$ oscillates with its characteristic wave period equal to $P = 50.7$ s for $x_0 = 2$ Mm, $P = 27.2$ s for $x_0 = 2.5$ Mm, and $P = 20.4$ s for $x_0 = 3$ Mm. These different wave periods result from different arcade lengths and different Alfvén speeds along the corresponding magnetic lines for $x_0 = 2$ Mm, $x_0 = 2.5$ Mm, and $x_0 = 3$ Mm.

We calculate a travel time of the Alfvén waves, $t_t$, for the first bounce along few magnetic field lines, which cross the given point $(x_0, y_0)$,

$$t_t = \int_0^l \frac{ds}{c_A(s)}. \quad (17)$$
Here, a coordinate along the magnetic line has the value of \( s = 0 \) at \((x_0, y_0)\), while for \( s = l \) the magnetic line ends at the transition region, \( y = 2.75 \) Mm. In Figure 11, the travel time is displayed depending on the initial point \( x_0 \). Its value gradually decreases with \( x_0 \), from \( t_1 \simeq 39 \) s at \( x_0 = 2 \) Mm and reaching \( t_1 \simeq 26 \) s at \( x_0 = 3 \) Mm. Because of the almost linear decrease of the magnetic field length from \( l = 23.4 \) Mm at \( x_0 = 2 \) Mm up to \( l = 11.6 \) Mm at \( x_0 = 3 \) Mm (not shown), these results show that the time of the Alfvén wave traveling along longer magnetic field lines is much bigger than for shorter magnetic lines. This effect is especially important in the case of the large arcade where the travel time falls off rapidly, contributing to the wave signal profile fanning.

Our results show the complex picture of Alfvén waves caused by wave reflection from the transition region, and the difficulties in direct studies of the interaction of counter-propagating waves in the asymmetric solar arcade. Because of these difficulties, we instead focus on evaluating a global attenuation time. This allows us to investigate integrally the attenuation processes affecting the transverse waves, like interactions of the counter-propagating waves, partial wave reflection from the transition region, and the wave energy leakage along a curved magnetic field line of the arcade.

### 4.3. Different Pulses Width

For a wider initial pulse, \( w_x \), the process of phase mixing becomes stronger. The reason for this is that both sides of such a pulse experience a larger phase difference due to a larger difference in the field line curvatures on both magnetic interfaces and the pulse deformation process in the transition region as compared to a narrower pulse. Hence, for the wider pulse, more strongly Alfvén wave propagation is affected.

Based on data signal of \( V_z \) collected at point \((x = 12 \) Mm, \( y = 7 \) Mm) for the case of a longer arcade \((x_0 = 2 \) Mm) and \((x = 9 \) Mm, \( y = 4.2 \) Mm) for the case of a shorter arcade \((x_0 = 3 \) Mm), we evaluate a wave period \( P \) using the fast Fourier transform method and an attenuation time \( \tau \). The ratio of attenuation time \( \tau \) to wave period \( P \) with respect to the width of the initial pulse is presented in Figure 12, which shows that \( \tau/P \) first increases for small values of \( w_x \) but then falls off slightly with \( w_x \).

When we look at the individual \( \tau/P \) versus the pulse width profiles of the two types of arcades, they exhibit a similar trend in which they increase up to a certain pulse width and then decrease. In the case of a more curved and larger magnetic arcade, the \( \tau/P \) first increases up to a 100 km pulse width (Figure 12, top panel), which means that up to this limit of the pulse width, the attenuation of the Alfvén waves decreases in the arcade.

Similarly, in the case of a less curved and smaller magnetic arcade, \( \tau/P \) first increases up to a 400 km pulse width (Figure 12, bottom panel), which means that up to this pulse width limit, the attenuation of the Alfvén waves decreases in the arcade. For \( w_x > 400 \) km, \( \tau/P \) decreases (Figure 12, bottom panel), which is the signature of the increment in wave attenuation. In other words, for the Alfvén waves launched with pulse widths larger than 400 km, the generated long wavelengths do not fit within the considered loop geometry and the wave leakage again causes wave attenuation (Gruszecki et al. 2007).

We also find that the attenuation of the Alfvén waves is smaller (larger the attenuation time with respect to the wave period) in the more curved and larger magnetic arcades \((x_0 = 2 \) Mm), while it is larger (smaller the attenuation time with respect to the wave period) in the case of the less curved and comparatively smaller arcades \((x_0 = 3 \) Mm). We found \( \tau/P = 1.75 \) s for the core of \( x_0 = 2 \) Mm and \( \tau/P = 1.89 \) s for \( x_0 = 3 \) Mm and for \( w_x = 0.2 \) Mm.

The arcade FWHM dependence on the position of the initial pulse \( x_0 \), and as a consequence of the size of the arcade, is shown in Figure 13, which clearly illustrates that a smaller arcade (bigger \( x_0 \)) has a smaller width (FWHM); a smaller arcade consists of weakly diverged magnetic field lines.

If one considers phase mixing to be the only candidate for the wave dissipation (e.g., Heyvaerts & Priest 1983), then the strong phase mixing in the more curved and larger arcades (see Figure 1) must cause a greater attenuation compared to the less strong phase mixing in the less curved and smaller arcades (see...
reflected in the transition region is smaller for Alfvén waves in
in Figure 14. We expect that the amplitude of the wave signal
for the first reflection from the transition region is presented
vital role in this phenomenon.

4.4. Partial Reflection from the Transition Region

Decay of the Alfvén wave amplitude results from wave
energy leakage caused by the curvature and divergence of
magnetic field lines, an inhomogeneous Alfvén speed \(c_A(x,y)\),
and partial penetration of the Alfvén wave signal into the
chromosphere (Gruszecki et al. 2007). We clearly observe in our
simulation that Alfvén waves experience partial reflection from
the transition region and the Alfvén wave signal penetrates into
solar atmospheric layers under the transition region (Figures 6
and 7, panels (d)–(h)). The amplitude of the waves penetrating
into the lower region of the atmosphere drops from about
\(V_x = 1 \text{ km s}^{-1}\) at \(t = 48 \text{ s}\) just under the transition region
(Figure 7(d)), to \(V_x = 0.5 \text{ km s}^{-1}\) after about 16 s (Figure 7(h)),
and finally disappears. We can evaluate the reflection coefficient,

\[
C_r = \frac{A_r}{A_i},
\]

where \(A_i\) (\(A_r\)) is the amplitude of the incident (transmitted)
waves. Substituting \(A_i = 6 \text{ km s}^{-1}\) and \(A_r = 4.01 \text{ km s}^{-1}\)
into the above formula, we get \(C_r = 0.668\), which means that 66.8\%
of the wave amplitudes became reflected in the transition region
and 33.2\% was transmitted into lower atmospheric layers. The
reflection coefficient, \(C_r\), versus the initial pulse position \(x_0\)
for the first reflection from the transition region is presented
in Figure 14. We expect that the amplitude of the wave signal
reflected in the transition region is smaller for Alfvén waves in
larger inclined magnetic field lines, which corresponds to larger
values of \(x_0\).

In the case of the largely curved arcades, the lateral leakage of
the Alfvén wave energy may also be largely dominant compared
to that associated with less curved arcades (Gruszecki et al. 2007).
The partial Alfvén wave reflection results from a steep gradient of the Alfvén speed in the transition region because of a significant mass density drop in this region of the solar atmosphere.

It must also be noted that in the case of linear Alfvén waves
generated by small initial velocity pulses, \(V_x = 3 \text{ km s}^{-1}\), with
the maximum amplitude reaching only \(V_x \approx 6 \text{ km s}^{-1}\), there are
no associated density variations.

5. SUMMARY AND CONCLUSIONS

To determine the role played by Alfvén waves in coronal
heating and solar wind acceleration, a number of authors have
investigated the physical processes responsible for the excitation
and attenuation of Alfvén waves in the solar atmosphere (e.g.,
Priest 1982; Ofman & Davila 1995; Ofman 2002; Miyagoshi
et al. 2004; Dwivedi & Srivastava 2006; Ofman & Wang 2007;
Chmielewski et al. 2013 and references therein). In general,
Alfvén waves have difficulty dissipating their energy and possi-
ble mechanisms involve collisional dissipative agents, such as
viscosity and resistivity, or non-classical plasma processes, such
as mode-coupling and phase mixing (see Heyvaerts & Priest
1983; Nakariakov et al. 1997; Zaqarashvili et al. 2006; Dwivedi
& Srivastava 2006 and references therein). Overall, collisional
dissipative processes are found to be less important for Alfvén
wave dissipation than the non-classical plasma processes, es-
pecially phase mixing (e.g., Nakariakov et al. 1997). Extensive
observational searches were performed to find the signatures
of Alfvén wave dissipation in the solar corona (e.g., Banerjee
et al. 1998; Harrison et al. 2002; O'Shea et al. 2005; Bemporad
& Abbo 2012 and references therein). However, as of today,
there is no convincing observational evidence for the existence
of Alfvén wave dissipation in the solar atmosphere.

In this paper, we simulated impulsively generated Alfvén waves in a stratified and magnetically confined solar arcade with the VAL-C temperature profile (Vernazza et al. 1981) as an initial realistic plasma condition in the curved magnetic field topology. Asymmetric solar magnetic arcades and Alfvén wave propagation in these arcades were modeled by time-dependent MHD equations that were solved numerically using the publicly available FLASH code (Lee & Deane 2009). We analyzed the effects of changing the horizontal position of the initial pulse and its width on the Alfvén wave propagation in the asymmetric solar arcade, the Alfvén wave deformation and phase mixing resulting from inhomogeneous Alfvén wave velocity, different lengths and divergence of magnetic field lines, and partial wave reflection in the solar transition region.

We found that the more curved and larger the arcade, the
stronger the attenuation of the Alfvén waves. Our results
also demonstrated that attenuation of Alfvén waves resulted

![Figure 13. Value of arcade FWHM vs. \(x_0\) for the chosen \(x = 11 \text{ Mm}\).](image)

![Figure 14. Reflection coefficient, \(C_r\), vs. \(x_0\).](image)
from the curvature and divergence of magnetic field lines, inhomogeneous Alfvén wave velocity, partial reflection in the solar transition region, and the decrement of the attenuation time of the Alfvén waves for wider initial pulses in the given magnetic configuration of various types of arcades. Moreover, our numerical simulations also showed that Alfvén waves, which are partially reflected in the solar transition region, return to the solar chromosphere as slowly downward propagating Alfvén waves.

The approach presented in this paper allowed us to investigate the effects caused by trains of Alfvén waves propagating in our arcade model as a result of the wave reflection in the solar transition region. Our results clearly show that the pulse deformation process in the transition region has a strong influence on Alfvén wave propagation and on wave damping in the curved magnetic field of the solar arcade together with the asymmetric magnetic field configuration, the plasma properties of the arcade, the horizontal size of the pulse, and the structure of the solar transition region.

In previous work, Nakariakov et al. (1999) investigated the transverse oscillations of EUV loops as observed by TRACE and demonstrated that the damping time was three times longer than the period of the oscillations. They considered kink oscillations of coronal loops and their damping caused by non-classical viscosity and resistivity. Then, Ofman et al. (2002) showed that the dissipation of Alfvén waves due to chromospheric wave leakage was not sufficient to describe such fast damping of the observed transversal oscillations in the solar atmosphere. Finally, Del Zanna et al. (2005) demonstrated that the dissipation of Alfvén pulses within their coronal arcade led to a change in the local Alfvén speed at various heights and depending upon the various localized conditions that determine the observed damping of these transverse oscillations.

In our work, the damping/attenuation time of the Alfvén waves are almost three times longer than those computed in both the longer and shorter arcades for a given pulse-width of 0.2 Mm. It should be noted that this damping time is due to Alfvén wave dissipation caused by phase mixing. The ratio of attenuation time and wave period is almost the same as what is observed for transverse wave dissipation in coronal loops. An important point that must be mentioned is that transverse kink waves with radial velocity perturbations in the cylindrical thin-tube geometry (Roberts 2000) are different than the Alfvén waves studied in this paper, which are essentially azimuthal. Nevertheless, there is a similar dissipation mechanism (e.g., phase mixing) that may work for these two types of waves; its efficiency highly depends on the localized plasma, magnetic field configuration, nature of wave drivers, Alfvén velocity, and other factors (see Ofman et al. 2002, 2007; Del Zanna et al. 2005). Therefore, our parametric studies presented in this paper provide some likely physical scenarios for the dissipation of Alfvén waves through phase mixing.

Finally, we would like to point out that our approach is significantly different from that developed by Del Zanna et al. (2005), who considered a symmetric coronal arcade embedded in the isothermal plasma with a constant (in time) temperature specified by the hyperbolic tangent profile, and designed in such a way that it described short-lived Alfvén waves in post-flare settings. Similarly, Miyagoshi et al. (2004) simulated Alfvén waves that were excited by perturbations imposed in the solar corona. By using our more realistic arcade model with an asymmetric magnetic field configuration, we were able to explore different physical aspects of the Alfvén wave propagation than those studied in the past. Essentially, our model significantly generalizes the model originally considered by Del Zanna et al. (2005) and by Miyagoshi et al. (2004). Nevertheless, further improvements to our model are possible and it is our hope that they would lead to an even better understanding of the inherent physical complexity of the phase mixing process and its role in the heating of the solar corona by Alfvén wave dissipation.

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