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QCD Resummation in Hard Diffractive Dijet Production at the Electron-Ion Collider

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Abstract. Diffractive dijet production at the electron-ion collider (EIC) has been proposed to study the gluon Wigner distribution at small-$x$. We investigate the soft gluon radiation associated with the final state jets and an all order resummation formula is derived. We show that the soft gluon resummation plays an important role to describe E791 data on $\pi$-induced diffractive dijet production at Fermilab. Predictions for the EIC are presented, and we emphasize that the soft gluon resummation is an important aspect to explore the nucleon/nucleus tomography through these processes.

Introduction. There have been renewed interests in hard diffractive dijet production in $e+p$ and $e+A$ collisions, which was one of the focuses of previous theoretical studies decades ago [1–9]. It was triggered by the possibility to explore the parton Wigner distributions in these processes [10–16]. The Wigner distributions of quarks and gluons [17, 18] represent an important aspect of the tomographic study for nucleons and nuclei in recent years, which is also one of the major focuses at the planned electron-ion colliders (EIC) [19–21].

One of the key observations in the new proposal is to measure the total transverse momentum of the dijet, the Fourier transform of which provides information on the coordinate space distribution of the partons. Together with the individual jet transverse momentum, this leads to a multi-dimensional tomographic picture of the nucleons and nuclei. Therefore, a precise measurement of the total transverse momentum distribution is of crucial importance to measure quark and gluon Wigner distribution functions.

Most previous analyses were based on the leading order picture of diffractive dijet production. To consolidate the factorization property of this process, we need to investigate higher order perturbative corrections [22, 23] and the relevant QCD evolution effects [15, 24]. In this paper, we will consider one of the important higher order contributions, i.e., all order soft gluon radiation associated with the final state jets. They can strongly affect the transverse momentum distribution of the dijet system at low momentum, and this should be taken into account when extracting the coordinate space distribution.

In order to change the dijet transverse momentum, the soft gluons have to be emitted outside the jet cones. They are therefore insensitive to the collinear singularity, and the relevant resummation becomes single logarithmic. It is known that such a resummation consists of two parts—the Sudakov logarithms and the so-called non-global logarithms (NGLs) [25–31]. The resummation of Sudakov logarithms is straightforward, and it will be interesting to compare their impacts in diffractive and non-diffractive processes. The resummation of NGLs, on the other hand, is known to be quite nontrivial, but to leading logarithmic approximation it can be done by using the existing techniques.

In our study, we will only consider color-neutral particles in the initial state (i.e., not a single quark or a gluon from the incoming hadrons) and color-singlet $t$-channel exchanges. At the EIC, the incoming electron radiates a virtual photon which diffractively scatters off the nucleon target and produces two final state jets. Another example are pion-induced coherent diffractive dijet processes, studied in fixed target experiments [32–41]. These two examples share strong similarities in the soft gluon radiation contributions and we will compare our resummation formula to existing data from the E791 experiment [33, 34]. This will provide a benchmark test to assess the applicability of our approach to diffractive dijet production at the EIC.

The rest of this paper is organized as follows. First, we will derive the soft gluon resummation contribution to the diffractive dijet production processes. We include both Sudakov and NGL contributions based on the Banfi-Marchesini-Smye (BMS) evolution equation [27]. Because of the universality of the soft gluon resummation, we apply our formula to the $\pi$-induced diffractive dijet processes. We will show that resummation plays an important role in the description of experimental data. We then apply our formalism for predictions at the EIC, where we will show the resummation effects on the momentum distribution and the azimuthal angular asymmetry. The latter is of particular interesting because it provides a novel correlation in the small-$x$ gluon Wigner distribution. Finally, we summarize our paper.

Soft Gluon Resummation in Diffractive Dijet Processes. We start with the leading order cross section of diffractive dijet production in $e+p$ and $e+A$ collisions

$$\frac{d\sigma}{d\Omega} = \int d^2\Delta_1 \int \frac{d\sigma_0}{dy_1 dy_2 dp_1 d^2\Delta_1} \delta^{(2)}(q_\perp + \Delta_1),$$

where $d\Omega = dy_1 dy_2 d^2 k_{1\perp} d^2 k_{2\perp}$ represents the phase space for the two final jets with rapidities $y_{1,2}$ and transverse momenta $k_{1\perp}$ and $k_{2\perp}$, respectively. $\vec{p}_1 = (\vec{k}_{1\perp} - \vec{k}_{2\perp})/2$ is the relative transverse momentum of the two jets and the total transverse momentum is de-
defined as \( \vec{q}_1 = \vec{k}_{1\perp} + \vec{k}_{2\perp} \). In the leading order kinematics, \( \vec{q}_1 = -\Delta_\perp \), where \( \Delta_\perp \) is the transverse component of the nucleon recoil momentum. In the so-called correlation limit, \( \vec{k}_{1\perp} \approx -\vec{k}_{2\perp} \), and we choose \( P_1 \sim |\vec{k}_{1\perp}| \sim |\vec{k}_{2\perp}| \gg |\vec{q}_1| \) to represent the jet transverse momentum. In the forward kinematics \( y_{1,2} \gg 1 \) which corresponds to the small-\( x \) region of the nucleon/nucleus, the cross section \( \sigma_0 \) can be written as the convolution of the hard kernel and the gluon Wigner distributions [11, 15].

In experiments, if the final state nucleon momentum \( P' \) can be re-constructed, one can directly measure the \( \Delta_\perp \)-distribution which provides information on parton distributions in impact parameter space. Alternatively, and complementarily, if one tries to reconstruct the \( \Delta_\perp \)-dependence from the measurement of the \( q_1 \)-distribution of the two jets, one has to take into account the additional soft gluon radiation contribution.

Due to the colorless exchange in the \( t \)-channel, the soft gluon radiation associated with the final state jets is very similar to that in jet production in \( e^+e^- \) annihilation. Typical one-gluon radiation diagrams are shown in Fig. 1. Since only the soft radiations emitted outside the jet cones count, the relevant resummation is single-logarithmic, of the sort studied in Ref. [25, 26] where large logarithms come from both the Sudakov and nonglobal effects. To leading logarithmic accuracy in the large-\( N_c \) approximation, the resummation of both these logarithms can be done by performing Monte-Carlo simulations [25, 26], or solving a differential equation called the BMS equation [27]. At finite \( N_c \), this can be done by the Langevin simulation of SU(\( N_c \)) matrices [30].

Taking into account the soft gluon radiation contributions, we can re-write the differential cross section as

\[
\frac{d\sigma}{d\Omega} = \int d^2\Delta_\perp \frac{d\sigma_0(y_1, y_2; P_1, \Delta_\perp) S(|q_1 + \Delta_\perp|)}{dy_1 dy_2 d^2P_1 d^2\Delta_\perp 2\pi|q_1 + \Delta_\perp|} = \int d^2\lambda_\perp \frac{d\sigma_0(y_1, y_2; P_1, \Delta_\perp) S(|\lambda_1|)}{dy_1 dy_2 d^2P_1 d^2\Delta_\perp 2\pi|\lambda_1|},
\]

where the soft factor \( S(|\lambda_1|) \) represents the probability, normalized as \( \int_0^{P_\perp} d\lambda_\perp S(\lambda_\perp) = 1 \), that the transverse momentum emitted outside the jet cones is less than \( \lambda_\perp \). This can be calculated from \( P(\tau) \), the probability that the transverse momentum emitted outside the jet cones is less than \( \lambda_\perp \) where

\[
\tau = \frac{N_c}{\pi} \int_{\lambda_\perp}^{P_\perp} d\lambda_\perp \frac{d\lambda_\perp}{N_\perp} \alpha_s(\lambda_\perp).
\]

\( S(\lambda_\perp) \) is related to \( P(\tau) \) via simple differentiation

\[
S(\lambda_\perp) = \frac{dP(\tau)}{d\lambda_\perp} = -\frac{N_c}{\pi\lambda_\perp} \alpha_s(\lambda_\perp) \frac{dP(\tau)}{d\tau}.
\]

Let us give simple analytical estimates of \( P(\tau) \) and \( S(\lambda_\perp) \). As long as \( \tau \) is not too large, which is usually the case in practical applications, \( P(\tau) \) is dominated by the Sudakov effects. Suppose that the two jets have the same rapidity \( y_1 = y_2 \) and are exactly back-to-back in azimuth \( \vec{k}_{1\perp} = -\vec{k}_{2\perp} \). Due to Lorentz invariance, one can boost this system to the center-of-mass frame of the dijet. Then, up to small corrections which stem from the difference between rapidity and angle variables around midrapidity, one finds

\[
P(\tau) \approx \exp \left( -\tau \ln \frac{1 + \cos R}{1 - \cos R} \right),
\]

where \( R \) is the jet radius. From this we immediately obtain

\[
S(\lambda_\perp) = \frac{\beta}{\pi\lambda_\perp^2} \left( \frac{\lambda_\perp^2}{\tau^2} \right)^\beta,
\]

where \( \beta = \frac{\alpha_s N_c}{2\pi} \ln \frac{1+\cos R}{1-\cos R} \). If we expand the above result in \( \alpha_s \), we find the following leading order result,

\[
S^{(1)}(\lambda_\perp) = \frac{\alpha_s N_c}{2\pi^2} \frac{1}{\lambda_\perp^2} \ln \frac{4}{R^2},
\]

in the small-\( R \) limit. This of course agrees with a direct calculation of the diagrams shown in Fig. 1 after identifying \( C_F \approx N_c/2 \) in the large-\( N_c \) limit.

Going beyond, we have calculated \( P(\tau) \) by numerically solving the BMS equation. The jets are placed back-to-back in azimuth \( \phi_2 = \phi_1 + \pi \), and each jet is delineated by a circle of radius \( R \) in the \((y, \phi)\) plane. \( P(\tau) \) then depends on \( R \) and the difference \(|y_1 - y_2|\). In order to facilitate the differentiation (4), we have fitted the result by the same analytical formula used in [25]. The result for \( R = 0.4 \) and \( y_1 = y_2 \) is,

\[
P(\tau) = \exp \left( -c_1 \tau - c_2 \tau^2 \frac{1 + (a\tau/2)^2}{1 + (b\tau/2)^2} \right),
\]

with \( c_1 = 3.32, c_2 = 1.01, a = 0.463, b = 0.459, c = 0.574 \). As expected, \( c_1 \) is rather close to the value \( \ln \frac{1+\cos 0.4}{1-\cos 0.4} \approx 3.19 \) found in Eq.(5). The \( c_2 \) term is due to the nonglobal logarithms.

Test of the resummation Formula in Pion Induced Diffraction. In early 2000s, the E791 experiment at Fermilab measured diffractive dijet production in pion-induced scattering [33, 34]. Its main purpose was to explore the color transparency phenomena of the nuclear
target (Platinum and Carbon) and novel parton distribution amplitude in pions [32]. To do that, the experiment also measured the total transverse momentum $q_{\perp}$ of the two jets to select the diffractive events. Therefore, the E791 experiment provides a unique opportunity to test our understanding of soft gluon radiation in diffractive dijet production processes.

Because of the nuclear targets, the diffractive events in E791 experiment contain both coherent and incoherent contributions. The former involves the whole nucleus and the latter involves nucleons in the nucleus. Accordingly, we can write the differential cross section as, approximately [37],

$$
\frac{d\sigma^A}{d^2\Delta_\perp} \propto \left[ A^2 e^{-\frac{q_{\perp}^2}{2\beta^2}} + A e^{-\frac{q_{\perp}^2}{8\beta^2}} \right],
$$

(9)

where $A$ is the nuclear number, and the first and second terms represent the coherent and incoherent diffractive contributions, respectively. In the above equation, $R_A \sim \frac{1}{13} R_p$ and $R_p$ are nuclear and nucleon radii.

In order to compute the $q_{\perp}$-distribution from Eq.(2), we convolute the $\Delta_\perp$ distribution of Eq.(9) with the soft factor of Eq.(4). In the E791 experiment, the jet transverse momentum is about 2 GeV and a special jet algorithm has been applied without an explicit jet size. Therefore, we decide to present our estimate by assuming $\beta \approx 0.6$ in Eq.(6), instead of an exact evaluation of $\beta$ which will depend on the jet size. This choice corresponds to a fixed coupling $\alpha_s = 0.3$ and $R \approx 0.25$. We can perform the convolution of Eq.(2) numerically, and find that the following analytic approximation for the final $q_{\perp}$ distribution describes the data well,

$$
d\frac{dN}{dq_{\perp}^2} = N P_{2\beta} (3 \frac{R_p^2}{R_A^2})^\beta \left[ \frac{1}{1 - \beta, 1, -\frac{q_{\perp}^2 R_A^2}{3}} \right] + A \left( 3 \frac{R_p^2}{R_A^2} \right)^\beta \frac{1}{1 - \beta, 1, -\frac{q_{\perp}^2 R_p^2}{3}}.
$$

(10)

The normalization factor $N$ depends on all other kinematic variables and $I_F_1$ is the Hypergeometric function.

In Fig. 2, we compare our results to the experimental data from E791. The coherent diffraction dominates at very low $q_{\perp}$, while the incoherent diffraction starts to take over at moderate $q_{\perp}$. On the other hand, at relative large $q_{\perp}$, the soft factor contribution dominates. We emphasize that the soft factor contribution is important for the whole kinematic region of $q_{\perp}$. Without it, we would not be able to describe the distributions, even at very small-$q_{\perp}$. We also compared our predictions to experimental data for the Carbon target, and found agreement using the same $\beta$ parameter. This indicates that the soft gluon radiation is the same as it should be, because it only concerns the jets in the final state.

We now turn to the jet transverse momentum dependence of the coherent diffractive events, where we show the comparison in the lower plot of Fig. 2. The experimental data are obtained by integrating over $q_{\perp}^2$ up to 0.015 GeV$^2$ [33, 34]. Because the $P_{\perp}$- and $q_{\perp}$-dependence are separated in Eq. (10), the $q_{\perp}$-integral will not affect the $P_{\perp}$-dependence. However, the additional factor of $P_{\perp}^{2\beta}$ of (10) will enter into final result. From the power counting analysis, the partonic differential cross section leads to a power behavior of $\frac{d\sigma}{dP_{\perp}^2} \sim 1/P_{\perp}^6$ [37–39]. By adding additional $P_{\perp}$-dependence in the associated gluon distribution functions [37] and the $1/P_{\perp}^{2\beta}$ from Eq. (10), we obtain the theoretical prediction as the solid curve in Fig. 2. The dotted curve are the predictions without soft

FIG. 2. Comparisons of the Sudakov effects in the total transverse momentum $q_{\perp}$ distribution (upper) and jet transverse momentum $P_{\perp}$ distribution (lower) for the diffractive dijet production in $\pi$-induced scattering on the nuclear target of Platinum with the experimental data from E791 Collaboration [33, 34]. The normalizations are arbitrary in the comparisons. In the upper plot, the dotted and dashed curves represent the coherent and incoherent diffractive contributions without soft factor, whereas the solid curve is the total contribution with soft factor. In the lower plot, the dashed curve represents the contribution without soft factor and the solid curve with soft factor.
factor contribution. As shown in Fig. 2, the predictions with soft factor have better agreement with the data.

Predictions for the Electron-Ion-Collider. The comparison between our theory predictions with previous E791 experiment demonstrates the importance of the soft factor contributions. In the following, we will present numeric results for cross sections measurable at a future EIC, focusing on coherent diffractive dijet production in $e + p$ collisions [10, 11, 15].

The cross section can be parametrized by azimuthal Fourier decomposition [15]

$$d\sigma_{L/T} = v_0 \left[ 1 + 2v_2 \cos 2\theta(P_{\perp}, \Delta_{\perp}) + \ldots \right]$$

(11)

where $\theta(P_{\perp}, q_{\perp})$ is the relative angle between dijet momentum $P_{\perp} = (k_{1,\perp} - k_{2,\perp})/2$ and the nucleon recoil $\Delta_{\perp}$, and $L(T)$ denotes a virtual photon with longitudinal (transverse) polarization. A non-zero $v_2$ in diffractive dijet production signals a non-trivial correlation between impact parameter and transverse momentum of the gluon Wigner distribution at small $x$ and is an important benchmark measurement for the EIC [15].

As discussed before, soft gluon radiation of the dijets which is not captured by the jet reconstruction, is an important issue to reconstruct Eq. (11). In the following, we consider all-order re-summation of soft-gluon radiation and investigate its effects both on the magnitude of the dijet production cross section as well as its elliptic azimuthal modulation.

To apply Eq. (2), we compute the leading order cross section $d\sigma_0$ from the Color Glass Condensate effective theory [42–46], including energy evolution by solving the leading order Jalilian-Marian-Iancu-McLerran-Weigert-Leonidov-Kovner JIMWLK equations numerically [47–50]. This part is the same as that computed in Ref. [15, 51], and more details can be found there.

A typical EIC kinematic is applied: $E_p = 250$ GeV for the proton beam energy, $W = \sqrt{(P + q)^2} = 140$ GeV for the center of mass energy and $Q^2 = 25$ GeV$^2$ for the photon virtuality. We consider symmetric u/d-flavor dijets with $z = \bar{z} = 0.5$, where $z = k_+^1/q^-$ is the longitudinal momentum fraction of the first jet relative to the photon and $\bar{z} = 1 - z$. In Fig. 3, we compare results of the total cross section $(\sigma_T + \sigma_L)$ from the CGC computation without final state radiation (for which $|q_\perp| = |\Delta_\perp|$) (black solid lines) with computations including soft radiation. The latter is obtained by employing Eq.(2) with the soft factor $S(\Lambda_{\perp})$ given by Eq.(4). We compare with three different coupling constant: $\alpha_s = 0.25$ (red dashed lines), 0.3 (blue dotted lines) and 0.35 (green dashed-dotted lines), respectively.

The effect of soft radiation on the cross section is similar to that in Fig. 2. The un-convoluted cross section falls steeply at larger $|q_\perp|$. Soft final state radiation reduces the cross sections by roughly a factor 5 – 10 in the back-to-back limit at small $|q_\perp|$. As the back-to-back peak is smeared by the soft radiation, the cross section at large $|q_\perp| \gtrsim 0.8$ GeV is larger than the un-convoluted one. To produce the results of Fig. 2 a coupling of $\alpha_s = 0.3$ was assumed. Here, we vary the coupling between $\alpha_s = 0.25 - 0.35$ to provide a systematic uncertainty of our results.

More importantly, the soft factor effects are different for the two contribution terms in the differential cross section of Eq. (11). Therefore, there will be net effects on the azimuthal modulation of $d\sigma/d|q_\perp|$. In Fig. 4, we show the azimuthal modulation $v_2$ of the total cross section $(\sigma_T + \sigma_L)$ as a function of $|q_\perp|$. In the presented kinematical regime, the $v_2$ obtained from the un-convoluted cross section, e.g. from $d\sigma/d|\Delta_\perp|$ (black stars), shows a strong modulation of up to $v_2 \approx 7\%$. In contrast, including soft gluon radiation significantly reduces the resulting azimuthal modulation of $d\sigma/d|q_\perp|$. Here, too we
show results for different values of $\alpha_s = 0.25, 0.3, 0.35$. At $\alpha_s = 0.3$ the maximal modulation is $v_2, L \lesssim 0.5\%$. Similar trends are observed when studying the transverse and longitudinal contributions separately. The rather strong lar trends are observed when studying the transverse and $\alpha$ parton Wigner distributions at the EIC.

It very difficult to measure for experiment. This means that the dijet total momentum cannot be a proxy for the recoiling proton momentum. Measuring the recoiled tar-

tal transverse momentum distribution for the

demonstrated that the soft factor from all order res-

Summary and Discussions. In this paper, we have demonstrated that the soft factor from all order re-

summation plays an important role to describe the to-

ation, a non-trivial gluon tomography at small-$x$.

In addition, we emphasize that the comparison be-

between the measurements in terms of $q^\perp_1$ and $\Delta^\perp_1$ (as shown in Figs. 3 and 4) provides a unique opportunity to study the QCD resumination effects, which can be compared to other jet production processes [25–31]. Finally, we point out that the extension to $e + A$ collisions at the EIC should be done accordingly, where we also have to take into account the coherent and incoherent diffraction contributions. We plan to address this in a separate publication.

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