Research Article

Practical Bipartite Tracking for Networked Robotic Systems via Fixed-Time Estimator-Based Control

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In this paper, the fixed-time practical bipartite tracking problem for the networked robotic systems (NRSs) with parametric uncertainties, input disturbances, and directed signed graphs is investigated. A new fixed-time estimator-based control algorithm for the NRSs is presented to address the abovementioned problem. By applying a sliding surface and the time base generator (TBG) approach, a new stability analysis method is proposed to achieve the fixed-time practical bipartite tracking for the NRSs. We also derive the upper bound of the convergence time for employing the presented control algorithm to solve the practical bipartite tracking problem and further demonstrate that the convergence time is independent of the initial value. Finally, the simulation examples are given to verify the effectiveness of the presented algorithms.

1. Introduction

Recently, the cooperative control of the networked robotic systems (NRSs) [1–4] has received increasing attention. The concept of the NRS is to denote a team of the controllable autonomous robots aiming to accomplish single or multiple global tasks over local communication. Compared with a single robot, the NRS is capable of achieving more complex missions in a more effective and flexible way. The distributed control algorithms of multiagent systems have been widely used to obtain various collective behaviors, including target tracking [5, 6], formation control [7–11], containment control [12, 13], distributed optimization [14, 15], distribution networks [16, 17], tracking performance limitations [18, 19], and resilient control [20] to name a few. Besides, many excellent control algorithms are proposed including observer-based adaptive control [21], fault-tolerant control [22], output feedback fuzzy control [23, 24], and fuzzy-approximation-based asymptotic control [25] to solve tracking problem for nonlinear systems. Note that all the abovementioned results are focused on networked systems with only cooperation. However, in some cases of real-world applications, the NRS is required to be divided into two subgroups and executes tasks from two opposite directions. This implies that the subgroups have to compete with each other. Therefore, it is of great significance to study the NRSs with both cooperation and competition.

Recently, bipartite consensus [26–28] and bipartite tracking [29–32] of multiagent systems involving both cooperation and competition have received increasing attention. Compared with conventional coordinated tracking behaviors, the bipartite tracking implies that all the robots converge to two opposite states of the leader with the identical state value and different signs. In [29], a class of bipartite tracking and containment control problems with signed digraphs has been addressed. Considering high-order multiagent system, bipartite tracking problems with uncertainties have been solved in [30]. The bipartite tracking problems subject to the time lag over matrix-weighted signed graphs for the NRSs have been studied in [31]. In [32], the bipartite tracking problems with a dynamic leader have been studied in linear multiagent system. It is worth mentioning that the aforementioned research mainly focused on first-, second-, and higher-order dynamics, as well as Lipschitz-type nonlinear systems. There are only a few results on bipartite tracking problems for the NRSs, and the control approaches for solving such problems are still lacked.

On the contrary, the convergence time is an important performance index in the field of distributed control. It thus motivates the development of the finite-time and the fixed-
time control to improve such convergence performance and, meanwhile, reject input disturbance [33, 34]. Different from the finite-time control, whose convergence time depends on the initial value [21, 35], the fixed-time control can force the states to reach the origin in fixed-time regardless of the initial value [36–42]. Due to such advantage, the fixed-time consensus for nonlinear heterogeneous multiagent systems has been studied in [37]. In [38], the fixed-time tracking for high-order multiagent systems has been taken into account. In [39], the fixed-time control has been applied to second-order nonlinear multiagent systems by integral sliding-mode approach. Especially, a time base generator (TBG) approach has been delivered to drive the states to approach a desired bounded range in fixed time through adjusting the TBG gain [40]. However, to the best knowledge of the authors, the fixed-time practical bipartite tracking problem for the NRSs remains open.

By the abovementioned discussions, this paper aims to provide a general solution to the fixed-time practical bipartite tracking problem for the NRSs with parametric uncertainties, input disturbances, and directed signed graphs. A fixed-time estimator-based control algorithm is designed to solve this problem. The main contributions of this work are threefold:

(i) Different from the control approaches for achieving the bipartite tracking of multiagent system [29–32], in which the system model is described by first-, second-, and higher-order dynamics, as well as Lipschitz-type nonlinear dynamics. The proposed control algorithms address the bipartite tracking problem of the networked robotic system, in which the dynamics of system is modeled by Euler–Lagrange equation, which is more meaningful to describe the actual physical agents.

(ii) Compared with the existing results on collective behavior of the NRS [3, 4], in which the convergence time is asymptotical, finite time, which is all related to the initial values of the system, the proposed fixed-time estimator-based control algorithm guarantees that the convergence time is fixed time, which is irrespective of the initial states of the system.

(iii) The presented control algorithm can provide a theoretical framework for stabilizing other complex uncertain networked systems in fixed time.

The remaining parts are organized as follows. Section 2 provides the preliminaries and the problem formulations. In Section 3, the fixed-time estimator-based control algorithm and its stability analysis are proposed. The simulation results are presented in Section 4 to test the algorithm. Finally, the conclusions are summed up in Section 5.

Notation: let $\mathcal{R}^N$ be the $N \times 1$ real matrix, $\mathcal{R}^{N \times N}$ be the $N \times N$ real matrix, $\text{diag} (\cdot)$ be the diagonal matrix, and $\text{sgn} (\cdot)$ be the sign function. $\text{sig} (x)$ is equal to $|x| \text{sgn} (x)$ with $l > 1$. $1_N = [1, 1, \ldots, 1]^T$ is the column vector of the $N$ dimension. $I_N$ is the $N$ dimension identity matrix. $(\cdot)_{\max}$ and $(\cdot)_{\min}$ are the maximum and minimum values of the given vector. $\lambda_{\min} (\cdot)$ is the minimum eigenvalues of the given matrix. Besides, $\| \cdot \|$ is the Euclidean norm.

2. Preliminaries

2.1. Graph Theory. The communication of the NRS can be modeled as a directed signed graph $\mathcal{G} = (\mathcal{V}, \mathcal{E}, h)$, where $\mathcal{V} = \{1, 2, \ldots , N\}$ is the set of vertexes, $\mathcal{E} \subseteq \mathcal{V} \times \mathcal{V}$ is the set of edges, and $\mathcal{E} = [a_{ij}] \in \mathcal{R}^{N \times N}$ is the adjacency matrix. An edge $e_{ij} \in \mathcal{E}$ (i.e., $a_{ij} \neq 0$) implies that the communication information flows directly from the vertex $j$ to the vertex $i$, otherwise $a_{ij} = 0$. $a_{ij} > 0$ implies that the vertex $i$ cooperates with the vertex $j$; $a_{ij} < 0$ implies that the vertex $i$ competes with the vertex $j$. Furthermore, assume that $\mathcal{G}$ has no self-loops, i.e., $a_{ii} = 0$. A directed path is denoted as a series of edges from $(1, 2), (3, 4), \ldots , (\eta - 1, \eta)$ with distinct vertexes and the length $\eta - 1$. A cycle of $\mathcal{G}$ is denoted as the starting and ending vertexes of the path being the same, namely, $\eta = 1$. Furthermore, if a cycle has even number negative weights, it is termed as positive cycle; otherwise, a cycle is referred to as a negative cycle. A directed signed graph includes a directed spanning tree, and it implies that there is a rooted vertex which has a directed path to any other vertexes. The Laplacian matrix of $\mathcal{G}$ is defined as $L_\mathcal{G} = \{l_{ij}\} \in \mathcal{R}^{N \times N}$ [26], where $l_{0i} = \sum_{j \neq i} a_{ij}$ and $l_{ji} = -a_{ij}, i \neq j$. A directed signed graph $\mathcal{G}$ is detail-balanced if there exist positive constants $h_1, h_2, \ldots , h_N$ such that $h_ia_{ij} = h_ja_{ji}$. A diagonal weighted matrix $B = \text{diag} (a_{10}, a_{20}, \ldots , a_{N0})$ represents the connection weight between the rooted robot and other robots. In detail, $a_{0i} > 0$ implies that the $i$th robot can directly receive the information from the rooted robot, otherwise $a_{0i} = 0$.

Definition 1 (see [26]). The directed signed graph is said to be structurally balanced if $\mathcal{G}$ can be grouped into two sets $\mathcal{G}^+$ and $\mathcal{G}^-$ satisfying $\mathcal{G} = \mathcal{G}^+ \cup \mathcal{G}^-, \mathcal{G}^+ \cap \mathcal{G}^- = \emptyset$ and $a_{ij} \geq 0, \forall v_i, v_j \in \mathcal{G}^0 (\partial \in \{+,-\}), a_{ij} < 0, \forall v_i, v_j \in \mathcal{G}^0, \partial \neq \emptyset (\partial, \partial \in \{+,-\})$.

Assumption 1. The directed signed graph $\mathcal{G}$ is structurally balanced and detail-balanced. The augmented graph $\mathcal{G}$ (including the graph $\mathcal{G}$ and the virtual leader) contains a directed spanning tree with the leader as the rooted vertex.

Lemma 1 (see [26]). A directed signed graph is structurally balanced if and only if there is a diagonal matrix $D = \text{diag} (d_1, d_2, \ldots , d_N)$ such that $D \mathcal{G}$ is positive semi-definite, where $d_i = 1$ if $v_i \in \mathcal{G}^+$ and $d_i = -1$ if $v_i \in \mathcal{G}^-$.

Lemma 2 (see [44]). Let $M_1 = L_\mathcal{G} + B$ and $M_2 = D M_1 D$. If Assumption 1 holds, there exists a positive-definite diagonal matrix $H = \text{diag} (h_1, h_2, \ldots , h_N)$ such that the matrix $M_2 H$ is positive definite.

2.2. Time Base Generator. The time base generator (TBG) [43] is defined as a function based on time satisfying predetermined restrictions on its initial and final values. Let the TBG gain be presented as follows:
where \( \xi(t) \) is the TBG and \( 0 < \delta \leq 1 \). For any given \( t_f > 0 \), we can design a proper TBG \( \xi(t) \) such that

1. \( \xi(t) \) is continuous and nondecreasing from \( \xi(0) = 0 \) to \( \xi(t_f) = 1 \), where \( t_f < +\infty \) is a scheduled time constant
2. \( \xi(0) = \xi(t_f) = 0 \), where the derivative of \( \xi(t) \) at \( t = 0 \) is actually its right derivative
3. \( \xi(t_f) = 1 \) and \( \xi(t_f) = 0 \) if \( t > t_f \)

**Lemma 3** (see [40]). Considering the following differential system,

\[
x(t) = -g(t)x(t), \quad x(0) = x_0,
\]

where TBG gain \( g(t) \) is defined in the form of (1) and \( x(t) \) denotes the state. Then, there exists a positive constant \( t_f > 0 \) with respect to \( \xi(t) \) in (1) such that \( \lim_{t \to +\infty} |x(t)| \leq 1 + \delta x_0 \) and \( |x(t)| \leq \delta/1 + \delta x_0 \) on \( t \in [t_f, +\infty) \), where \( \delta \) is given in (1).

**Remark 1.** An example of the TBG is presented as follows [40]:

\[
\xi(t) = \begin{cases} 
\frac{10}{t_f^2} - \frac{24}{t_f} + \frac{15}{t_f^2}, & 0 \leq t \leq t_f, \\
1, & t > t_f,
\end{cases}
\]

where \( t_f > 0 \) is a positive constant and denotes the user-designed convergence time, which is an important parameter to ensure the convergence of the states before the time \( t_f \). Then, the main techniques to design the TBG function is to satisfy four properties given in (1). A typical TBG function with \( t_f = 4 \) is shown in Figures 1 and 2 to enhance its visualization.

### 2.3. System Formulation

The dynamics of the ith robot in the NRS is presented below [36]:

\[
M_i(q_i){\ddot q}_i + C_i(q_i, {\dot q}_i){\dot q}_i + g_i(q_i) + d_i(t) = \tau_i,
\]

where \( t \geq 0, \ i \in \mathcal{F} \), \( q_i, {\dot q}_i, {\ddot q}_i \in \mathbb{R}^n \) are, respectively, the generalized position, velocity, and acceleration, \( M_i(q_i) \in \mathbb{R}^{n \times n} \) stands for the positive-definite inertia matrix, \( C_i(q_i, {\dot q}_i) \in \mathbb{R}^{n \times n} \) is the centrifugal-Coriolis matrix, \( g_i(q_i) \in \mathbb{R}^n \) represents the gravitational term, \( d_i(t) \in \mathbb{R}^n \) is the input disturbances satisfying \( \sup_{t \geq 0} |d_i(t)| \leq d_M \), \( d_M \) is a positive constant, and \( \tau_i \in \mathbb{R}^n \) denotes the control input.

The parameters of the dynamical model can be described as

\[
M_i(q_i) = M_{i0}(q_i) + \Delta M_i(q_i),
C_i(q_i, {\dot q}_i) = C_{i0}(q_i, {\dot q}_i) + \Delta C_i(q_i, {\dot q}_i),
g_i(q_i) = g_{i0}(q_i) + \Delta g_i(q_i),
\]

where \( M_{i0}(q_i), C_{i0}(q_i, {\dot q}_i), \) and \( g_{i0}(q_i) \) are the desired parts of the dynamic model and \( \Delta M_i(q_i), \Delta C_i(q_i, {\dot q}_i), \) and \( \Delta g_i(q_i) \) are the uncertain term of the dynamic model. Therefore, system (4) can be rewritten as

\[
M_{i0}(q_i){\ddot q}_i + C_{i0}(q_i, {\dot q}_i){\dot q}_i + g_{i0}(q_i) = \tau_i + \rho(t),
\]

where \( \rho(t) = -\Delta M_i(q_i){\ddot q}_i - \Delta C_i(q_i, {\dot q}_i){\dot q}_i - \Delta g_i(q_i) - d_i(t) \). Following [36], \( \rho(t) \) is upper bounded, namely,

\[
\|\rho(t)\| \leq b_0 + b_1\|{\dot q}_i\|^2 + b_2\|{\dot q}_i\|,
\]

where \( b_0, b_1, b_2 > 0 \). On the contrary, the leader’s states \( q_0, v_0, \) and \( u_0 \in \mathbb{R}^n \) obey that \( q_0 = v_0 = u_0 = 0 \).

**Assumption 2.** The acceleration of the leader is upper bounded, i.e., \( \sup_{t \geq 0} \|u_0(t)\| \leq u_{\text{max}} \).

### 2.4. Problem Formulation

The control objective is to design a proper control input \( \tau_i \) for achieving the practical bipartite tracking of the NRS in a fixed time. Denote \( q_i, v_i \) as the position and the velocity of the followers. Then, a useful definition and Lemma 4 are listed as follows.

**Definition 2.** The practical fixed-time bipartite tracking problem is addressed if there exists a constant \( T \) regardless of the initial value of the states such that \( \lim_{t \to +\infty} \|q_i(t) - q_0(t)\| \leq \rho_1, \lim_{t \to +\infty} \|v_i(t) - v_0(t)\| \leq \rho_2, \|q_i(t) - q_0(t)\| \leq \rho_1, \|v_i(t) - v_0(t)\| \leq \rho_1, \) and \( \|v_i(t) - v_0(t)\| \leq \rho_2, \) on \( t \in [T, +\infty) \), \( \forall i \in \mathcal{F}^+ \), and \( \lim_{t \to +\infty} \|q_i(t) + q_0(t)\| \leq \rho_1, \lim_{t \to +\infty} \|v_i(t) + v_0(t)\| \leq \rho_1, \) and \( \|v_i(t) + v_0(t)\| \leq \rho_2, \) on \( t \in [T, +\infty) \), \( \forall i \in \mathcal{F}^+ \), \( \forall i \in \mathcal{F}^- \), where \( \rho_1, \rho_2 > 0 \) can be sufficiently small by choosing appropriate control parameters.

**Lemma 4** (see [33]). For the nonlinear system \( \dot{x} = f(x), x(0) = x_0, x \in \mathbb{R}^n \). Suppose that there exist a positive-definite and continuous function \( V(x) \), real numbers \( \alpha, \beta > 0, \gamma_1 < 1, \) and \( \gamma_2 > 1 \) such that \( V(x) + aV^{\gamma_1}(x) + \beta V^{\gamma_2}(x) \leq 0 \). Then, the origin is the fixed-time stable
equilibrium point of the considered system. The setting time is given as
\[
T \leq T_{\text{max}} = \frac{1}{\alpha(1 - p_1)} + \frac{1}{\beta(y_2 - 1)},
\]  

(8)

Remark 2. In missile guidance, hitting the target within a specified time and its predefined neighborhood is a demanding objective. Compare with the traditional control approaches, which can only achieve asymptotic, exponential, and finite-time stability, because the value of their convergence time depends on the initial condition. Besides, for the complex network, it is very difficult to deal with the switched information between the cyber layer and the physical layer. In the paper, we employ the estimator-based control algorithm to deal with information of each layer. It is a feasible plan for complex cyber-physical system to simplify the proof and make the system stable within fixed time.

Remark 3. The estimator-based control approach is early employed to target the tracking problem of the networked robotic system in [6]. Based on this idea, the predefined-time formation tracking problem of networked surface vehicles [7], the multiformation tracking problem of networked heterogeneous robotic systems [11], and lag-bipartite tracking problem of networked robotic systems [31] have been successfully addressed. It thus believes that the proposed control algorithm can be generalized to other systems and other tracking control problems.

3. Main Results

3.1. Fixed-Time Estimator-Based Control Algorithm. In this section, the fixed-time estimator-based control algorithm for achieving practical bipartite tracking of the NRS is proposed. Before constructing the control input, we design the following sliding-mode surface:
\[
s_i(t) = \hat{q}_i + K_1 \phi_1(\hat{q}_i) + K_2 \hat{q}_i, \tag{9}
\]
where \( \hat{q}_i(t) \) is the estimated state with respect to \( q_i(t) \) and \( \hat{q}_i \) is the estimated value of \( q_i \). The control law is designed as
\[
\begin{aligned}
\tau_i &= \tau_{i0} + \tau_{i1} + \tau_{i2}, \\
\tau_{i0} &= M_{i0}(q_i, \hat{q}_i) \hat{q}_i + C_{i0}(q_i, \hat{q}_i) \hat{q}_i + g_{i0}(q_i), \\
\tau_{i1} &= -K_{i1} \text{sgn}(s_i) - M_{i0}(q_i)(K_{i2} \text{diag}(\nabla \phi(q_i)) + K_{i2} \text{diag}(\nabla \phi(\hat{q}_i))) \hat{q}_i, \\
\tau_{i2} &= -s_i ||\hat{q}_i|| T_{\text{aux}}, \\
T_{\text{aux}} &= \frac{1}{1 - b_2} \left( k + b_0 + ||\hat{q}_i||^2 + b_2 \|\tau_{i0} + \tau_{i1}\| \right),
\end{aligned}
\]

(12)

\[
\begin{aligned}
\hat{q}_i(t) &= -\left( \eta_1(t) + 1\right) \left( \sum_{j=1}^{N} a_{ij} \left( \hat{q}_i(t) - \text{sgn}(a_{ij}) \hat{q}_j(t) \right) + a_{i0} \left( \hat{q}_i - d_i q_0 \right) \right) \\
&+ \hat{v}_i(t) - c_1 \text{sgn} \left( \sum_{j=1}^{N} a_{ij} \left( \hat{q}_i(t) - \text{sgn}(a_{ij}) \hat{q}_j(t) \right) + a_{i0} \left( \hat{q}_i - d_i q_0 \right) \right), \\
\hat{v}_i(t) &= -\left( \eta_2(t) + 1\right) \left( \sum_{j=1}^{N} a_{ij} \left( \hat{v}_i(t) - \text{sgn}(a_{ij}) \hat{v}_j(t) \right) + a_{i0} \left( \hat{v}_i - d_i v_0 \right) \right) \\
&- c_2 \text{sgn} \left( \sum_{j=0}^{N} a_{ij} \left( \hat{v}_i(t) - \text{sgn}(a_{ij}) \hat{v}_j(t) \right) + a_{i0} \left( \hat{v}_i - d_i v_0 \right) \right),
\end{aligned}
\]

(13)
where (12) represents the local control layer and (13) stands for the estimator layer, \( K_{\alpha} \) is the positive-definite diagonal matrix, \( r > 1, k, c_1 \) and \( c_2 \) are positive constants, \( h_{\text{max}} = \max\{h_1, \ldots, h_N\} \), \( h_{\text{min}} = \min\{h_1, \ldots, h_N\} \), and the TGB gains \( \eta_1(t) \) and \( \eta_2(t) \) are defined as

\[
\eta_1(t) = \frac{h_{\text{max}} \dot{x}_1(t)}{2 \lambda_{\text{min}}((M_D H) \otimes I_N)(1 - \xi_1(t) + \delta_1)}.
\]

\[
\eta_2(t) = \frac{h_{\text{max}} \dot{x}_2(t)}{2 \lambda_{\text{min}}((M_D H) \otimes I_N)(1 - \xi_2(t) + \delta_2)}.
\]

Taking the time derivative of \( s_i \) and multiplying both sides of the equation by \( M_{\alpha}(q_i) \), we have

\[
M_{\alpha}(q_i) \dot{s}_i = M_{\alpha}(q_i) \tilde{q}_i + M_{\alpha}(q_i) \left( K_{\alpha} \text{diag}\{V(\phi(\tilde{q}_i))\} + K_{\beta} \text{diag}\{\xi(\tilde{q}_i)\}\right) \tilde{q}_i.
\]

Then, substituting \( M_{\alpha}(q_i) \tilde{q}_i \) from (6) in (15) yields

\[
M_{\alpha}(q_i) \dot{s}_i = r_i + \rho(t) - M_{\alpha}(q_i) \tilde{q}_i - C_0(q_i, \tilde{q}_i) \tilde{q}_i - g_0(q_i) + M_{\alpha}(q_i) \left( K_{\alpha} \text{diag}\{V(\phi(\tilde{q}_i))\} + K_{\beta} \text{diag}\{\xi(\tilde{q}_i)\}\right) \tilde{q}_i.
\]

Denote \( \tilde{e}_i(t) = \tilde{q}_i(t) - d_i q_0 \) and \( \tilde{e}_i(t) = \dot{e}_i(t) - d_i v_0 \). Substituting the proposed cascade control input equation \( r_i \) into (16) yields the following cascade closed-loop system:

\[
\begin{cases}
\dot{s}_i = M_{\alpha}(q_i)^{-1} \left( \frac{k + b_0 + b_1 \|q_i\|^2 + b_2 \|r_{\alpha} + r_{\text{gi}}\|}{1 - b_2} \dot{s}_i + \rho(t) - K_{\alpha} \text{sgn}(s_i) \right), \\
\dot{e}_i(t) = -\left( \eta_1(t) + 1 \right) \left( \sum_{j=1}^{N} a_{ij} \left( \tilde{e}_j(t) - \text{sgn}(a_{ij}) \tilde{e}_j(t) \right) + a_{ji} \tilde{e}_j(t) \right) + \dot{e}_i(t) - c_1 \text{sgn}(m_{ij}(\tilde{e}_j(t) - \text{sgn}(a_{ij}) \tilde{e}_j(t)) + a_{ji} \tilde{e}_j(t)), \\
\dot{e}_j(t) = -\left( \eta_2(t) + 1 \right) \left( \sum_{j=1}^{N} a_{ij} \left( \tilde{e}_j(t) - \text{sgn}(a_{ij}) \tilde{e}_j(t) \right) + a_{ji} \tilde{e}_j(t) \right) - c_2 \text{sgn}(m_{ij}(\tilde{e}_j(t) - \text{sgn}(a_{ij}) \tilde{e}_j(t)) + a_{ji} \tilde{e}_j(t)) - d_i u_0(t).
\end{cases}
\]

Obviously, the fixed-time practical bipartite tracking problem for the NRSs is solved if the closed-loop system (17) is fixed-time stable.

3.2. Stability Analysis for the Distributed Estimator Layer

We focus on the convergence analysis of the distributed estimator layer. It is worthy to point out two positive constants \( T_{\jmath 1} \) and \( T_{\jmath 2} \) can be arbitrarily determined by selecting proper TBG. Besides, \( \xi_1(t) \) and \( \xi_2(t) \) are predefined in (14).

The position error is represented in the form of \( \tilde{e}(t) = [\tilde{e}_1(t), \tilde{e}_2(t), \ldots, \tilde{e}_N(t)]^T \). The velocity error is in the form of \( \bar{e}(t) = [\bar{e}_1(t), \bar{e}_2(t), \ldots, \bar{e}_N(t)]^T \). Let \( \tilde{e}(t) = (D \otimes I_N) \tilde{e}(t) \), \( \bar{e}(t) = (D \otimes I_N) \bar{e}(t) \), then, we can construct the following Lyapunov function candidate:

\[
V_1(t) = \frac{1}{2} \left( ((M_D H) \otimes I_N) \bar{e}(t) \right)^T ((M_D H) \otimes I_N)^{-1} \left( ((M_D H) \otimes I_N) \bar{e}(t) \right),
\]

\[
V_2(t) = \frac{1}{2} \left( ((M_D H) \otimes I_N) \bar{e}(t) \right)^T ((M_D H) \otimes I_N)^{-1} \left( ((M_D H) \otimes I_N) \bar{e}(t) \right).
\]

Denote \( [z_{ij}]_{N \times N} = (M_D^T H^{-1}) \otimes I_N \). Let \( z_{\text{min}} = \min\{z_{ii} + \sum_{j \neq i} z_{ij} : z_{ii} + \sum_{j \neq i} z_{ij} \neq 0, \forall i, j \in N \} \), \( \min\{[z_{ij}] : z_{ij} \neq 0, i \neq j, \forall i, j \in N \} \).

Theorem 1. Suppose that Assumptions 1-2 hold. If

\[
0 < \delta_1, \delta_2 \ll 1, \xi_1(t) \text{ and } \xi_2(t) \text{ denoting TGB and } M_D, \text{ and } H \text{ is defined in Lemma 2.}
\]

Taking the time derivative of \( s_i \) and multiplying both sides of the equation by \( M_{\alpha}(q_i) \), we have

\[
M_{\alpha}(q_i) \dot{s}_i = M_{\alpha}(q_i) \tilde{q}_i + M_{\alpha}(q_i) \left( K_{\alpha} \text{diag}\{V(\phi(\tilde{q}_i))\} + K_{\beta} \text{diag}\{\xi(\tilde{q}_i)\}\right) \tilde{q}_i.
\]
where $\delta_1$ and $\delta_2$ are presented in (14). It is equivalent to that $\tilde{q}_i$ and $\tilde{v}_i$ converge to an arbitrarily small neighborhood of the leader's state bilaterally within a bounded convergence time.

Next, for the given following Lyapunov function candidate $V_2(t)$, where the matrix $H$ is defined in Lemma 2. Differentiating $V_2(t)$ along (21) yields

$$V_2(t) = ((M_D \otimes I_n)\tilde{x}(t))^T ((M_D H) \otimes I_n)^{-1} ((M_D \otimes I_n)\tilde{e}(t))$$

$$= -(\eta_2(t) + 1) \left( ((M_D \otimes I_n)\tilde{x})^T (H^{-1} \otimes I_n) ((M_D \otimes I_n)\tilde{e}) - ((M_D \otimes I_n)\tilde{x})^T (H^{-1} \otimes I_n) (c_2\text{sgn} ((M_D \otimes I_n)\tilde{e}) - 1_N \otimes u_0) \right)$$

$$\leq - (\eta_2(t) + 1) h_{\text{max}}^{-1} \| (M_D \otimes I_n)\tilde{x} \|^2 - c_2 h_{\text{max}}^{-1} \| (M_D \otimes I_n)\tilde{e} \|^2 - c_2 h_{\text{max}}^{-1} \| (M_D \otimes I_n)\tilde{e} \|^2$$

$$\leq - 2\eta_2(t) h_{\text{max}}^{-1} \lambda_{\text{min}} ((M_D H) \otimes I_n) V_2(t) + (N u_{\text{max}} h_{\text{max}}^{-1} - c_2 h_{\text{max}}^{-1}) \| (M_D \otimes I_n)\tilde{e} \|^2 \leq - \frac{\dot{\xi}_{\text{e}}(t)}{1 - \xi_1(t) + \delta_2} V_2(t).$$

For $t \in [0, T_{f_1}]$, by using Lemma 3, $V_2(t)$ converges to a residual set $\Omega_2 = \{ V_2(t) | V_2(t) \leq \delta_1/2 + \delta_2 V_2(t) \}$ at a pre-specified time $T_{f_1}$ independent of initial states of robots, so $\lim_{t \to T_{f_1}} \| \tilde{e}(t) \| \leq 1/N \sqrt{2\delta_2/\lambda_{\text{min}} ((1 + \delta_2) V_2(t))}$, which is equal to $\lim_{t \to T_{f_1}} \| \tilde{e}(t) \| \leq 1/N \sqrt{2\delta_2/\lambda_{\text{min}} ((1 + \delta_2) V_2(t))}$. It indicates that the velocity error can converge to a desired level so long as $\delta_2$ is chosen properly in protocol. Moreover, $T_{f_1} + T_{f_2}$, where $T_{f_1}$ and $T_{f_2}$ are the user-designed parameters in the TBG gains $\eta_1$ and $\eta_2$ presented in (14), following the definition of $g(t)$ and $t_f$ provided in Section 2.2.

**Proof.** The proof is processed in two steps. In the first step, according to (17), the compact form of the velocity error is obtained as $\tilde{e} = -\eta_1(t) (M_D \otimes I_n)\tilde{e} - (M_D \otimes I_n)\tilde{e}(t) - c_2\text{sgn} ((M_D \otimes I_n)\tilde{e}(t)) - (D \otimes I_n) (1_N \otimes u_0)$. Since $DD = I_N$, one can obtain that

$$\tilde{e} = - (\eta_2(t) + 1) (M_D \otimes I_n)\tilde{e} - c_2\text{sgn} ((M_D \otimes I_n)\tilde{e}) - 1_N \otimes u_0.$$
It thus follows from (22) that \( \| \vec{v}_i(t) \| \leq 1/N \sqrt{2\delta_i}/z_{\min} (1 + \delta_i) V_1 (0), \forall t > T_{f_i} \), and the practical convergence error is disposed by sign function. For \( t \in [T_{f_i}, T_{f_i} + T_{f_2}] \), using Lemma 3, one draws a conclusion that \( V_1(t) \) decreases to a set of residuals \( \Omega_1 = \{ V_1(t) | V_1(t) \leq \delta_i/1 + \delta_i V_1(0) \} \) at \( T_{f_i} + T_{f_2} \), that can be attained independent with initial states. Furthermore, one obtains that 

\[ \lim_{t \to T_{f_i} + T_{f_2}} \| \vec{v}_i(t) \| \leq 1/N \sqrt{2\delta_i}/z_{\min} (1 + \delta_i) V_1 (0), \]

which is equal to 

\[ \lim_{t \to T_{f_i} + T_{f_2}} \| \vec{v}_i(t) \| \leq 1/N \sqrt{2\delta_i}/z_{\min} (1 + \delta_i) V_1 (0). \]

This means that the position state error can be predesigned as a required level so long as an appropriate \( \delta_i \) is applied in \( \eta_1(t) \). Hence, \( \| \vec{v}_i(t) \| \leq \sqrt{2\delta_i}/z_{\min} (1 + \delta_i) V_1 (0), \forall t > T_{f_i} + T_{f_2} \) and \( \lim_{t \to T_{f_i} + T_{f_2}} \| \vec{v}_i(t) \| = 0. \) That is, \( \vec{q}_i \to \vec{q}_0, \forall i \in \Omega \). This completes the proof.

Remark 4. From Lemma 3, it obtains that the solution of (2) is \( x(t) = \xi_0 (1 - \xi(t)/1 + \delta). \) According to property of \( \xi(t) \), it implies that \( \xi(t_f) = 1; \) it thus obtains that 

\[ \lim_{t \to t_f} | x(t) | \leq \delta/1 + \delta \xi_0. \]

When \( \delta \) is small enough, the influence of the initial state is negligible. It thus implies that \( x(t) = 0 \) when \( t \geq t_f \), namely, the fixed-time convergence can be achieved by using the TBG-based approach.

Remark 5. It is worth noting that the closed-loop system \( s_i = \vec{q}_i - \vec{v}_i + \delta_i + K_{i1} \phi \left( \vec{q}_i \right) + K_{i2} \sigma \left( \vec{q}_i \right) \), where \( \delta_i \) is the tiny error in the convergence procedure. Based on the above analysis, \( \vec{q}_i \) can be approximately replaced by \( \vec{v}_i \) as \( t > T_{f_1} + T_{f_2} \). It is unnecessary that we employ \( \delta_i \) in the stability analysis. Therefore, we employ the simplified closed-loop system \( s_i = \vec{q}_i - \vec{v}_i + K_{i1} \phi \left( \vec{q}_i \right) + K_{i2} \sigma \left( \vec{q}_i \right) \) in the subsequent analysis for avoiding redundant proof.

3.3 Stability Analysis for the Fixed-Time Practical Bipartite Tracking for the NRSs. In this section, the stability analysis for the proposed fixed-time estimator-based control algorithm is studied.

**Theorem 2.** Considering the robot dynamic system with parametric uncertainties and input disturbances described by (4), the input torque \( \tau_i \) ensures that \( q_i \) and \( \dot{q}_i \) globally converge to an user-defined small set \( \Delta \) within a fixed time \( T_s + T_c \), where \( T_s \) and \( T_c \) are derived as follows:

\[ T_s \leq \frac{2}{\sqrt{m_1 + m_2}} \left( \frac{1}{k} + \frac{n^{(r - 1)/2}}{(r - 1)\lambda_{\min}(K_{11}) (m_1 + m_2)^r} \right), \]

\[ T_c \leq \frac{2(1 - p)^{1/2}}{(1 - p)\lambda_{\min}(K_{11})} + \frac{(2n)^{1/2}}{(1 - l)\lambda_{\min}(K_{22})}. \]

This implies that the fixed-time practical bipartite tracking problem can be solved in the fixed time \( T \leq T_s + T_c + T_{f_1} + T_{f_2} \), where \( T_{f_1} \) and \( T_{f_2} \) are user-defined parameters, as presented in Theorem 1.

**Proof.** The Lyapunov function candidate was chosen as follows:

\[ V = \frac{1}{2} s_i^T M_{i0} (q_i) s_i. \]

Taking the derivative of \( V \) with respect to time along (16), we obtain

\[ \dot{V} = s_i^T M_{i0} (q_i) \dot{s}_i. \]

After substituting \( \dot{s}_i \) from the first equation of (17) into (28),

\[ \dot{V} = s_i^T \left( -\frac{k + b_0 + b_1 \| \dot{q}_i \|}{(1 - b_2)} \| s_i \| \right) s_i + \rho - K_{i0} \sigma \left( s_i \right). \]
Denote $s_{ij}$ as the $j$th element of the $s_i$; substituting (7) into (29), it follows that

$$
\dot{V} \leq -b_2 \|s\| r_{\max} - \|s\| \left( k + b_0 + b_1 \|\tilde{q}\|^2 + b_2 \|r_0 + r_1\| \right) + \|s\| \left( b_0 + b_1 \|\tilde{q}\|^2 + b_2 \|r_1\| \right) - s_i^T K_{0i} \sigma' \left( s_i \right)
$$

$$
\leq -s_i^T K_{0i} \sigma' \left( s_i \right) - k \|s\| - b_2 \|s\| r_{\max} + b_2 \|s\| r_{\max}
$$

$$
\leq -\lambda_{\min} (K_{0i}) \sum_{j=1}^{n} |s_{ij}|^{r+1} - k \|s\|
$$

$$
\leq -n^{(1-r)/2} \lambda_{\min} (K_{0i}) \|s\|^{r+1} - k \|s\|.
$$

Suppose that $m_1 \leq \|M^{-1} (q_i)\| \leq m_2$. Choosing $M_{i0} = 2/m_1 + m_2 I_n$ [45], we have

$$
V = \frac{1}{m_1 + m_2} \|s\|^2.
$$

(31)

Applying (31) to (30), it follows that

$$
V + k \sqrt{m_1 + m_2} \sqrt{V} + n^{(1-r)/2} \lambda_{\min} (K_{0i}) (m_1 + m_2)^{(r+1)/2} V^{(r+1)/2} \leq 0.
$$

(32)

By Lemma 4, it obtains that $s_i$ converge to zero when $t \rightarrow T^*_t$, which is predefined in (25). After the sliding surface $s_i = 0$ is achieved within $T^*_t$, the system dynamics are converted to $\dot{\tilde{q}}_i = -K_{1i} \phi' (\tilde{q}_i) - K_{2i} \sigma' (\tilde{q}_i)$. Then, the convergence of $\tilde{q}_i$ can be settled by the following two cases.

Case 1 ($\|\tilde{q}_i\| \geq \Delta$): the dynamics can be explicitly simplified as $\dot{\tilde{q}}_i = -K_{1i} \phi' (\tilde{q}_i) - K_{2i} \sigma' (\tilde{q}_i)$. Choose the Lyapunov function candidate defined by Case 1, we obtain

$$
\dot{V}_{calc} = -\tilde{q}_i^T \dot{\tilde{q}}_i
$$

$$
= -\tilde{q}_i^T K_{1i} \phi' (\tilde{q}_i) - \tilde{q}_i^T K_{2i} \sigma' (\tilde{q}_i)
$$

$$
\leq -\lambda_{\min} (K_{1i}) \|\tilde{q}_i\|^{r+1} - n^{(1-r)/2} \lambda_{\min} (K_{2i}) \|\tilde{q}_i\|^{r+1}
$$

$$
\leq -2 \left( \frac{1}{2} \right) \lambda_{\min} (K_{1i}) V_{calc}^{(r+1)/2} - 2 \left( \frac{1}{2} \right) n^{(1-r)/2} \lambda_{\min} (K_{2i}) V_{calc}^{(r+1)/2}.
$$

(33)

Invoking Lemma 4 again, the tracking error $\tilde{q}$ converges to the arbitrary small $\Delta$ within the time $T^*_t$ given by (26).

Case 2 ($\|\tilde{q}_i\| < \Delta$): applying (10), the dynamics can be definitely simplified as $\dot{\tilde{q}}_i = -p\Delta^{-1} K_{1i} \tilde{q}_i - K_{2i} \sigma' (\tilde{q}_i)$. Selecting the appropriate Lyapunov function candidate defined by Case 1, we obtain

$$
\dot{V}_{calc} = -p\Delta^{-1} \tilde{q}_i^T K_{1i} \tilde{q}_i - \tilde{q}_i^T K_{2i} \sigma' (\tilde{q}_i) \leq -2p \Delta^{-1} \lambda_{\min} (K_{1i}) V_{calc}.
$$

(34)

It is obvious seen that the tracking errors $\tilde{q}_i$ exponentially converge to zero.

Remark 6 It is of great significance that we introduce a linear term in the function $\phi (\tilde{q}_i)$ for the case of $\|\tilde{q}_i\| \leq \Delta$. Otherwise, the control design with $\phi (\tilde{q}_i)$ may generate singularity problem due to the first derivative of $\phi (\tilde{q}_i)$ including a negative power $(p-1)$ on $\tilde{q}_i$, which may go to infinity while $x$ goes to zero. This may lead to the desired control cost infinity.

4. Simulation Results

In this section, simulation experiments are carried out to verify the effectiveness of the proposed algorithm. Assume that the NRS contains eight two-DOF robotic manipulators with interactions displayed in Figure 3.

The communication mode includes one leader and two subnetworks. There only exist cooperative relationships among the robots in each subnetwork by the solid lines, while there are the competitive relationships between the two subnetworks by the dotted lines. Besides, there are an even number of negative weights in each loop. It thus obtained that Assumption 1 holds. In addition, bidirection communication between two vertexes stands for different information delivered between two robots.
Furthermore, we propose a simple application of our control strategy, in which two parts of robots cooperate and compete with each other to avoid obstacles in the task. In the phase 1, the robots cooperate with each other and track the target before detecting the obstacle. In the phase 2, when the robots detect obstacles, the eight robots which have both cooperative and competitive relationships can be split into two clusters to bypass the obstacle. In the phase 3, the robots cooperate with each other and track the target again after passing the obstacle.

In the practical application, the communication data are determined by the hardware setting of the communication system. However, in the theoretical research, we need to employ the communication data of the directed signed system. However, in the theoretical research, we need to employ the communication data of the directed signed graph to verify the effective of the control algorithm.

The physical parameters of the eight robotic manipulators are listed in Table 1, where $m_k, k \in \{1, 2\}$, stands for the masses of links, $l_k$ represents the lengths of links, $r_k$ is the center of the link’s mass, and $J_k$ represents the moment of inertia of links.

The initial conditions of robots are chosen as $q(0) = [q_{10}^T, q_{20}^T]^T$, $\nu(0) = [\nu_{10}^T, \nu_{20}^T]^T$, $\bar{q}(0) = [\bar{q}_{10}^T, \bar{q}_{20}^T]^T$, and $\bar{\nu}(0) = [\bar{\nu}_{10}^T, \bar{\nu}_{20}^T]^T$, where

\[
\begin{align*}
q_{10} & = [3, -2, -2, 3, -2, -2, 3, -2]^T, \\
q_{20} & = [-2, 3, -1, 2, 3, -1, 2, 3]^T, \\
\nu_{10} & = [-1, -3, 2, -1, -3, 2, -1, -3]^T, \\
\nu_{20} & = [-3, 6, -5, -7, 3, 1, -2, 7]^T, \\
\bar{q}_{10} & = [1, 2, -3, 1, 2, -3, 1, 2]^T, \\
\bar{q}_{20} & = [-1, 8, 5, -7, 1, -3, 2, 4]^T, \\
\bar{\nu}_{10} & = [-1, -3, 2, -1, -3, 2, -1, -3]^T, \\
\bar{\nu}_{20} & = [2, 2, -3, 2, 2, -3, 2, 2]^T.
\end{align*}
\]  

\[ (35) \]

The position, velocity, and acceleration states of the leader are, respectively, selected as $q_0 = [\sin(t); \sin(t)]^T$, $\nu_0 = [\cos(t); \cos(t)]^T$, and $u_0 = [-\sin(t); -\sin(t)]^T$. The control parameters are given as $\rho = 0.5, q = 1.2, r = 1.5, k = 1, b_0 = 12, b_1 = 2.8, b_2 = 0.5, \delta_1 = \delta_2 = 0.01, c_1 = 0.01, c_2 = 1,$

| ith robot | $m_k$ (kg) | $l_k$ (m) | $r_k$ (m) | $J_k$ (kg·m²) |
|-----------|------------|-----------|-----------|-------------|
| 1         | 1.32, 1.08 | 2.76, 2.48| 1.38, 1.24| 0.84, 0.55  |
| 2         | 1.23, 1.02 | 2.64, 2.42| 1.32, 1.21| 0.71, 0.50  |
| 3         | 1.26, 1.04 | 2.68, 2.44| 1.34, 1.22| 0.75, 0.52  |
| 4         | 1.32, 1.08 | 2.76, 2.48| 1.38, 1.24| 0.84, 0.55  |
| 5         | 1.23, 1.02 | 2.64, 2.42| 1.32, 1.21| 0.71, 0.50  |
| 6         | 1.26, 1.04 | 2.68, 2.44| 1.34, 1.22| 0.75, 0.52  |
| 7         | 1.32, 1.08 | 2.76, 2.48| 1.38, 1.24| 0.84, 0.55  |
| 8         | 1.23, 1.02 | 2.64, 2.42| 1.32, 1.21| 0.71, 0.50  |

$K_{01} = \text{diag}(4, 3), K_{11} = \text{diag}(2, 2), \text{ and } K_{21} = \text{diag}(2, 2)$. The input disturbance $d(t) = 0.1[\cos(t); \sin(t)]^T$. From Figure 1, the Laplacian matrix $L_s$ is

\[
L_s = \begin{bmatrix}
3 & 0 & 0 & -2 & 1 & 0 & 0 & 0 \\
0 & 2.5 & -0.5 & -1 & 0 & 1 & 0 & 0 \\
0 & -1 & 1 & 0 & 0 & 0 & 0 & 0 \\
-0.5 & -0.5 & 0 & 2 & 0 & 0 & 1 & 0 \\
0.5 & 0 & 0 & 0 & 1.5 & 0 & 0 & -1 \\
0 & 0.5 & 0 & 0 & 0 & 2.5 & -2 & 0 \\
0 & 0 & 0 & 0.5 & 0 & -1 & 2 & -0.5 \\
0 & 0 & 0 & 0 & -0.5 & 0 & -1 & 1.5
\end{bmatrix},
\]

(36)

where $B = \text{diag}(0, 1, 0, 0, 0, 1, 0, 0)$ and $H = \text{diag}(2, 1, 2, 0.5, 1, 0.5, 0.25, 0.5)$.

Based on the aforementioned parameter setting, the simulation results of the proposed algorithms are shown in Figures 4–9. From Figures 4 and 5, it is shown that the robots’ position and velocity states are divided into two groups to track the leader’s trajectory, where robots belonging to subnetwork A converge to the states of the leader within the predesigned time, while the robots belonging to subnetwork B approach to the opposite state of the leader within the predesigned time. In Figures 6–8, the tracking errors are, respectively, provided to illustrated the tracking performances of the position states. From Figure 7, the
Figure 4: Pictures (a) and (b) reveal the evolution of $q_i$ for links 1 and 2, respectively. Pictures (c) and (d) reveal the evolution of $\dot{q}_i$ for links 1 and 2, respectively.

Figure 5: Continued.
Figure 5: Pictures (a) and (b) reveal the evolution of $v_i$ for links 1 and 2, respectively. Pictures (c) and (d) reveal the evolution of $\dot{v}_i$ for links 1 and 2, respectively.

Figure 6: Pictures (a) and (b) reveal the evolution of the position tracking errors for links 1 and 2.
Figure 7: Pictures (a) and (b) reveal the evolution of the errors $\tilde{e}_i$ for links 1 and 2.

Figure 8: Continued.
estimators $\tilde{q}_i$ can track the neighbourhood of leader state $q_0$ within $T_{f_1} + T_{f_2}$, which proves the effectiveness of the estimator layer. From Figure 8, the true value $q_i$ can converge to the neighbourhood of estimators $\tilde{q}_i$ within $T_s + T_c$, which demonstrates the effectiveness of the local control layer. In Figures 6 and 9, the tracking errors $e_i$ and $\dot{e}_i$ converge to the
neighbourhood of the origin within the convergence time $T$, which indicate the effectiveness of the proposed algorithms.

5. Conclusion

In this paper, the fixed-time practical bipartite tracking problem for the NRSs has been investigated under parametric uncertainties, input disturbances, and directed signed graph. A new fixed-time estimator-based control algorithm is proposed to solve this problem. Some necessary conditions are established. The validity of the proposed algorithm was demonstrated in the simulation graph. Future work will concentrate on bipartite tracking problem with uniform time delay and input saturation.

Data Availability

No data were used to support this study.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

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