ASTF: Visual Abstractions of Time-Varying Patterns in Radio Signals

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Abstract—A time-frequency diagram is a commonly used visualization for observing the time-frequency distribution of radio signals and analyzing their time-varying patterns of communication states in radio monitoring and management. While it excels when performing short-term signal analyses, it becomes inadequate for long-term signal analyses because it cannot adequately depict signal time-varying patterns in a large time span on a space-limited screen. This research thus presents an abstract signal-time-frequency (ASTF) diagram to address this problem. In the diagram design, a visual abstraction method is proposed to visually encode signal communication state changes in time slices. A time segmentation algorithm is proposed to divide a large time span into time slices. Three new quantified metrics and a loss function are defined to ensure the preservation of important time-varying information in the time segmentation. An algorithm performance experiment and a user study are conducted to evaluate the effectiveness of the diagram for long-term signal analyses.

Index Terms—Radio signal, visual abstraction, time-oriented data, binary sequence

1 INTRODUCTION

A radio signal is an electromagnetic wave used to transmit and receive information through space [58]. Radio signals vary in their center frequencies and bandwidths because a radio signal must occupy a contiguous section of the electromagnetic spectrum. As the spectrum is a finite natural resource and there has been a rapid growth in radio devices, the demand for the spectrum has continuously increased. Therefore, radio communications must be supervised by radio administration bureaus to ensure orderly spectrum usage [17, 65].

In radio monitoring and management, time-frequency (TF) diagrams are commonly used to visualize radio spectrum data that are captured by spectrum sensing equipment and formatted in frequency frames [4, 18]. A typical TF diagram is shown in Fig. 1. Its y-axis and x-axis represent the time and frequency, respectively. A blue band indicates the electromagnetic amplitudes at the corresponding time-frequency points are higher than environmental noise and may be occupied by a radio signal for communication. For example, through viewing the TF diagram in Fig. 1, three radio signals can be found from left to right. The first signal is constant with high strength. The second signal communicates for nearly one minute. The third signal has low strength and occurs twice for a short time.

The daily work of radio supervisors includes short-term (e.g., 3−5 minutes) and long-term (e.g., 1−2 days or 1−2 weeks) signal analyses. In short-term analyses, they often rapidly acquire signal details at a specific time or in real-time, such as the number of signals, the center frequency and bandwidth of a signal, or the communication state and strength of a signal. However, in long-term analyses, they are mainly concerned with the changing patterns of communication states and strength, which may indicate a signal’s behavior. TF diagrams excel at performing short-term analyses but become inadequate for long-term analyses. The main reason is that directly rendering long-term radio spectrum data on a space-limited screen will result in overplotting. Therefore, short discontinuities (i.e., a constant signal disappears for a moment) or short communications (i.e., a signal appears for a short time then disappears) could not be visible, which possibly causes the misjudgment of signal behaviors. Taking the signal S6 in Fig. 2 as an example, it communicates for the entire day, but occurs a few short discontinuities around 11:40 (Fig. 2(b-1)). However, these discontinuities are not visible in Fig. 2(a-1) because overplotting causes many frequency frames to be covered.

Overplotting can be partly addressed using animation, scrolling, aggregation, or sampling; however, each of these solutions has challenges. Animation and scrolling cannot directly provide a comprehensive picture over time, so radio supervisors must patiently browse an entire time span to reconstruct the time-varying patterns of signals [5, 16, 39, 49], as the scrolling TF diagram illustrated in Fig. 2(b). In addition, aggregation and sampling inevitably cause the loss of information [21, 30]. Finding a proper aggregation or sampling strategy to preserve short discontinuities and short communications is challenging. For example, the discontinuities of the signal S6 around 11:40 are also not visible in the aggregated TF diagram shown in Fig. 2(c-e-1), because the duration of each of these discontinuities is less than the threshold of aggregation rendering in this case.

This research thus presents a new diagram, i.e., Abstract Signal Time-Frequency (ASTF) diagram, that is tailored to long-term radio signal analyses. As shown in Fig. 2(d), the ASTF diagram depicts the time-frequency distribution of 10 signals and their time-varying patterns in 1 day. The ASTF diagram also indicates the occurrences of short discontinuities (Fig. 2(d-1 and d-2)), short communications (Fig. 2(d-3 and d-4)), and signal anomalies (Fig. 2(d-4)). Its design consists of three parts, namely, a data processing (Section 4), a visual abstraction method (Section 5), and a time segmentation algorithm (Section 6).

During the data processing (Fig. 3(a−d)), radio spectrum data are converted into radio signal data formatted in multidimensional signal records, a set of binarized signal communication state sequences, and a set of signal anomaly records using classic signal processing methods. The radio signal data provide the basic characteristics, namely, center frequency, bandwidth, strength, and signal-to-noise ratio (SNR), of radio signals over time. A binary sequence records the communication states of a signal over time, where logic “1” and logic “0” represent appearing and disappearing states, respectively. Anomalies provide information about abnormal characteristic values of signals, such as sudden frequency shifts or abrupt strength impulses.
ASTF’s visualization design (Fig. 3(e-h)) adopts the idea of visual abstraction that preserves valuable information while removing meaningless details in data for large-scale data visualizations [2]. A new visual abstraction method is proposed on the basis of dividing the entire period of a binary sequence into \( n \) slices, and the timeline in a display into \( n \) cells, to form a one-to-one sequential correspondence. First, ASTF’s basic layout maps signal basic characteristics into a 2D plane with reference to typical TF diagrams. Then, a set of visual encodings for a cell are designed to abstractly represent the communication state changes of a signal in a slice. Lastly, two visual cues are used to highlight anomalies occurring in a signal.

To ensure that the information needed in long-term signal analyses is well preserved in the visual abstraction, a new time segmentation algorithm, i.e., Binary Sequence Segmentation for Visual Abstraction (BSSVA), is created. Three new quantified metrics are used in the algorithm to measure the preserved information in the visual abstraction. A loss function is also derived to optimize the time segmentation.

An algorithm performance experiment and a user study were conducted to demonstrate the effectiveness of the BSSVA algorithm and ASTF diagram (Section 7). The performance experiment results showed that the algorithm had fewer information losses than five reference algorithms. The user study results found that participants were more accurate and took less time when using ASTF diagrams to complete long-term radio signal analysis tasks compared to scrolling and aggregated TF diagrams.

In summary, this paper contributes 1) an ASTF diagram that supports long-term radio signal analyses and 2) a visual abstraction method and a BSSVA time segmentation algorithm that can be applied to long-term binary sequence visualizations.

2 RELATED WORK

2.1 Radio Communication Visualizations

Visualizing radio communications is an interdisciplinary domain. Existing studies can be categorized into three well-known visualization subfields, namely, scientific visualization [13, 36], information visualization [12, 46], and visual analysis [19, 65], based on the diversity of data sources and analytical tasks.

Scientific visualization is mainly used for visualizing electromagnetic field simulation data [13, 27, 51]. Users can, for example, intuitively observe the radiation range of electromagnetic waves of radio devices for performance validations [54, 67].

Information visualization is mainly applied to visualize radio spectrum data. Our approach belongs to this subfield. Classic spectrograms, such as amplitude-time (AT), amplitude-frequency (AF), and TF diagrams, have been widely used in commercial spectrum analyzers [4, 18]. Researchers have introduced advanced interactions and novel visualizations into these diagrams. Kincaid [34] used Focus+Context interactions in AT diagrams for analyzing long-lived signals. Hernandez et al. [42] introduced a time-wrap and 2.5D-layered method into AT diagrams to visualize long-lived signals. While these approaches improve the scalability of AT diagrams in terms of time, they are unsuitable for TF diagrams because radio spectrum data are visualized by lines in AT diagrams but by bitmaps in TF diagrams. Sharakhov et al. [47] and Cantu et al. [11] adopted 3D visualizations to present multidimensional information in TF diagrams. Zhao et al. [65] proposed a new diagram to visualize multiple characteristics of signals. These approaches improve the usability of TF diagrams by enabling them to present multidimensional information but have weak time scalability. ASTF, however, uses a visual abstraction method and a time segmentation algorithm to improve the time scalability of TF diagrams.

Visual analysis aims to solve complex analytical tasks, such as signal behavior analysis [19] and electromagnetic situation awareness [65]. Their main features include multi-source data, advanced data processes, and multi-viewed interactive interfaces. ASTF has the potential to become a common component in such visual analysis systems because it could act as a superior view that provides an overall picture of long-term radio spectrum data.

Fig. 2. Illustrations of four visualizations of radio spectrum data with 86,400 frequency frames in 1 day with an interval of 1 second. The display area for visualizing the data has 900 \( \times \) 300 pixels. (a) A typical TF diagram visualizes the entire data in the display area, wherein a pixel is rendered 288 times. (b) A scrolling TF diagram visualizes the data with a paging mode using a scrolling bar, wherein 288 pages are filled and each of them contains 300 frequency frames (i.e., 5 minutes). (c) An aggregated TF diagram visualizes the entire data in the display area, wherein the timeline is evenly divided into 300 segments and each of the segments represents the aggregated communication state and strength of a signal in 288 seconds. In this case, a segment will be rendered with color if the proportion of appearing states is larger than 50% over 288 seconds. Otherwise, the segment remains blank. The color represents the mean strength of a signal over 288 seconds. (d) Our proposed ASTF diagram visualizes the entire data.
Fig. 3. Pipelines of data processing (a−d) and visualization design (e−h). In the data processing pipeline, (a) radio spectrum data formatted in frequency frames are converted into (b) radio signal data formatted in multidimensional data records, then (c) binarized communication state sequences are extracted from and (d) anomalies are detected in the radio signal data. In the visualization pipeline, (e) a TF diagram is commonly used for visualizing short-term radio spectrum data, and an ASTF diagram is newly designed for visualizing long-term radio signal data via three steps: (f) mapping multi-dimensional characteristics of signals into a 2D plane to form the basic layout of ASTF, (g) depicting the time-varying patterns of communication states of signals by using a proposed visual abstraction method and a new time segmentation algorithm, and (h) highlighting anomalies with visual cues.

2.2 Visual Abstractions of Time-Oriented Data

Time-oriented data may have a wide range of values and large time spans [49], which results in overplotted and cluttered visualizations. Visual abstraction is an important time-oriented data visualization technique that visually encodes important information and removes unnecessary details [2]. Existing approaches can be divided into three categories by visual channels, namely, position, color, and area [1, 9].

Positional visual encodings map positions in a long-time axis into a limited display area using hierarchical or juxtaposed methods. For example, ChronoLenses [63], Stack Zooming [29], and TimeNotes [55] layer a large time span with levels of details on demand. Small multiples are a juxtaposed method that visualizes a large time span with juxtaposed sub-spans. Color visual encodings use colors to map a wide range of values into several value levels (e.g., Heatmap [1, 38], Horizon Graph [45], and Calendar Graph [35]). Area visual encodings use shapes with different acreages to map a large time span or a wide value range into a visual space (e.g., Icicle plots [37, 53], Sunburst plots [59], and Multi-resolution techniques [8, 25]). Application systems often combine two or three categories to fulfill specific analytical requirements [26, 35]. For example, Aigner et al. [3] proposed a composite visual encoding method based on the three categories to visualize the blood glucose data of diabetes patients. In the present work, the proposed abstraction method is also a coordinated use of these three categories to fulfill long-term radio signal analysis requirements.

2.3 Time Segmentation Methods

In data mining, time segmentation divides a time sequence into appropriate segments for feature engineering [41, 60], similarity search [31, 56], data compression [44], and visual abstraction [7, 8]. Existing algorithms can be classified into five strategies [32, 43]. Equal-length division (EL) [32] divides a sequence into subsequences of equal length. It requires a negligible time cost with a given segment number n but ignores changes and trends in the sequence. Bottom-up (BU) [33, 43] strategies divide a sequence with detected feature points, such as turning or extreme points. They incur a mid-level time cost and are highly effective in reserving changes or trends, but the number of segments is uncertain.

Each of these strategies has advantages and disadvantages. In real-world usage, users should select the proper one or even combine strategies in accordance with target application scenarios. For example, Zhang et al. [62] used perceptually important points to implement an FP approach to preserve trends in a stock time series. Keogh et al. [33] used an SW strategy within a BU-based approach to reduce BU’s time cost. The present work combines the EL and FP strategies to create a new time segmentation method for long-term radio signal analyses.

3 DESIGN REQUIREMENTS

The target users of this research are radio supervisors who are responsible for supervising radio communications within an area (e.g., an airport or a harbor). Two radio supervisors from a radio spectrum management agency were involved in the entire process of this study. TF diagrams are their main visualization tools for observing and analyzing radio spectrum data in their daily work. They propose several requirements for long-term radio signal analyses, which can be translated into visualization requirements below.

R1. Present explicit information about radio signals. Radio spectrum data record the amplitudes of frequency points but do not directly provide signal characteristics. In short-term analyses, radio supervisors can estimate signal characteristics by observing TF diagrams; however, in long-term analyses, the time span enlarges and the number of signals increases, leading to a considerable cognition burden. Therefore, new diagrams should explicitly present a signal’s characteristics.

R2. Reveal the time-varying patterns of radio signals. Radio supervisors have different concerns in short- and long-term analyses. In short-term monitoring, they often acquire signal details. However, in long-term analyses, they are concerned with a signal’s changing patterns of communication states and strength. Therefore, new diagrams should reveal such patterns and ignore unnecessary details.

R3. Highlight anomalies within radio signals. Anomalies may happen on any signals and often occur over a short time. For example, center frequency shifts may occur when intense noises interfere. Impulse strength peaks may occur when the equipment is unstable. Such anomalies cannot be easily observed in TF diagrams. New diagrams should thus highlight anomalies and depict their distribution over time.
4 Data Processing
To fulfill these requirements, radio spectrum data are processed using three steps, i.e., signal identification, communication state inspection, and anomaly detection.

4.1 Signal Identification
Signal identification [23, 61] is a historical and evolving field that focuses on extracting explicit signal information from radio spectrum data (R1). In this work, classic signal identification methods recommended by our users are adopted to process radio spectrum data with an interval of 1 second. Compared with semi-structured radio spectrum data, the processed radio signal data are fully structured as multidimensional records (Fig. 3(b)). A record consists of a timestamp, signal ID, and the four basic characteristics of a signal (i.e., center frequency, bandwidth, strength, and SNR). Records with the same signal ID represent the same radio signal.

4.2 Communication State Inspection
A radio signal has two communication states, i.e., appearing and disappearing. The two states indicate whether a signal is or is not communicating at a specific time. As radio signal data do not provide this state information, the communication state of a signal at each timestamp needs to be inspected using its characteristics in radio signal data (R2). Based on suggestions from our users, when the strength of a signal in the last 5 seconds is higher than environmental noise, the signal is in the appearing state (i.e., “1”), otherwise it is in the disappearing state (i.e., “0”). Consequently, the communication states of a signal in a period are represented by a binary sequence with an interval of 1 second (Fig. 3(c)).

4.3 Anomaly Detection
Anomalies are statistical outliers of signal characteristics, such as frequency shifts and strength impulses. Many existing anomaly detection methods [6, 64, 66] may be feasible to detect the four types of anomalies (R3) in accordance with the four basic characteristics of a signal. Considering that anomaly detection is not the focus of this paper, we directly adopt classic Pauta criteria [20, 48] suggested by our users for anomaly detection. For example, the criterion for detecting bandwidth anomalies is that the bandwidth of a signal at a timestamp exceeds the range of \((\mu \pm 3\sigma)\), where \(\mu\) and \(\sigma\) are the average and standard deviation of bandwidth in the period (Fig. 3(d)).

5 Visualization Design
The visualization design of the ASTF diagram consists of three aspects, i.e., signal characteristics visualization (R1), visual abstractions of signal time-varying patterns (R2), and anomaly visualization (R3).

5.1 Signal Characteristics Visualization
The ASTF diagram is designed to visualize radio signal data that provide signal basic characteristics over time. Therefore, the basic characteristic visualization maps the multidimensional information of signals into a 2D plane (R1).

Using the basic layout of TF diagrams and the habits of our users (R4), the \(x\) and \(y\) axes are frequency and time, respectively (Fig. 3(f)). A straight stripe along the \(y\)-axis represents a signal. The stripe’s width and midpoint on the \(x\)-axis represent the signal’s bandwidth and center frequency, respectively. In general, the center frequency and bandwidth of a signal are constant, and small fluctuations can be ignored in long-term analyses. If large fluctuations occur, they will be detected as anomalies and encoded by visual cues (Section 5.3). The color of a stripe represents the strength. As specific strength values of a signal are unnecessary details during long-term analyses, three strength levels, i.e., high, medium, and low, are used and encoded with blues of different saturations using user-provided thresholds (e.g., -50 dBm and -70 dBm used in this work). These colors are commonly used in spectrum sensing equipment (R4). The SNR is not mapped because it is usually proportional to the strength.

5.2 Visual Abstractions of Signal Time-Varying Patterns
The time-varying patterns of a signal refer to its changing patterns of strength and communication states in a period (R2). The changing patterns of strength are presented using the three-level color encoding method from Section 5.1. This section introduces how to visualize the changing patterns of communication states.

As the communication states of a signal over time are a binary sequence, two types of communication state change points (CSCPs) exist, i.e., rising edge (from disappearing to appearing) and falling edge (from appearing to disappearing), as illustrated in Fig. 3(c). Therefore, the communication states can be represented by a CSP distribution over time, which contains the number of communications and the starting and ending time of each communication.

Aggregation is a feasible solution to visualize long-term signal time-varying patterns in a space-limited screen, as illustrated in Fig. 2(c). However, this solution may result in two problems. First, it is difficult to set a proper proportion of appearing states to determine whether a segment should be rendered. A large proportion results in the loss of short communications and a small proportion causes the loss of short discontinuities. For example, Signal S10 has two short discontinuities from 16:00 to 20:00, but only one can be perceived in Fig. 2(c-2). Signal S7 has several short communications from 3:00 to 5:00, but only two short communications are shown in Fig. 2(c-3). Second, if the changes in communication states happen at a certain frequency, several lines or rectangles will be sequentially painted with small gaps (e.g., Signal-01 in Fig. 3(f) and Signal S2 in Fig. 2(c-4)). Such a situation will cause a moiré effect [10, 57], an optical illusion where lines or rectangles align, which will interfere with visual perception.

To overcome these problems, a visual abstraction method is proposed (Fig. 3(g)). The method consists of three steps.

**STEP 1. Conducting segmentation in data and visual spaces.** A radio signal coexists in data and visual spaces. The data space is the binary communication state sequence. The visual space refers to the stripe representing the signal in an ASTF diagram. This step divides the binary sequence into \(n\) time slices and the stripe into \(n\) painting cells. The \(n\) slices and \(n\) cells form a one-to-one sequential correspondence for visual abstraction. Thus, a small cell in visual space conveys the valuable information contained in the corresponding slice that covers a large time span in data space.

Data space segmentation needs to obtain an optimal \(n\) and determine the time span of each slice. The algorithm we propose to handle this is explained in Section 6.

Visual space segmentation needs to determine the size of a cell and the range of \(n\). In terms of cell size, the width of a cell is determined by the bandwidth of the signal. The length of a cell is equal to the division of the total length of the time axis into \(n\). That is, all cells in a stripe have the same length to facilitate the subsequent steps. In terms of the range of \(n\), we suggest determining it by the size of the painting area in a display from two considerations. First, the search space of optimal \(n\) in data space should be limited to a range to reduce the time cost. Second, a large \(n\) will generate small-sized cells resulting in low recognizability in visual space, whereas a small \(n\) will generate large-sized cells leading to information loss. We conducted pilot studies to obtain an empirical range for mainstreaming displays with a 2K resolution (i.e., [30, 50]).

**STEP 2. Classifying CSPC distributions in data space.** CSPC distributions vary in time slices. If the total number of CSCPs and the type and occurrence time of each CSPC in a slice are considered, visual abstraction would be impossible due to intractable classes of CSPC distributions. We thus propose a method to classify CSPC distributions into a handful of classes.

The classification method includes an agreement and three bases. The agreement is that if a CSPC occurs at the dividing point of two
adjacent slices, it should belong to the slice where the signal appears (Fig. 4(a)). This ensures that a CSCP is only included in one slice. The three bases are the number level of CSCPs, the type of the first CSCP, and the type of the last CSCP in a slice. Using this classification method, ten classes of CSCP distributions are obtained (Fig. 4(b)). Class1 and Class2 have no CSCP, indicating that a signal keeps the same state. Class3 and Class4 have only one CSCP, indicating that a signal changes its state once. Class5 and Class6 have two CSCPs, indicating two state changes. Class5 is a rising-first-falling-second pattern, while Class6 is a falling-first-rising-second pattern. The four remaining classes have more than two CSCPs, presenting falling-first-falling-last (Class7), rising-first-rising-last (Class8), rising-first-falling-last (Class9), and falling-first-rising-last (Class10) patterns.

**VERule2:** For a slice with only one CSCP, the cell is (Cell2) or is not (Cell1) filled depending on whether the signal is appearing (Class2) or disappearing (Class1) in the slice.

**VERule3:** For a slice with two CSCPs, Class5 is a rising-first-falling-second pattern that conveys two messages: the signal is not communicating when entering and leaving the slice but completes a short communication within this slice. We also use two sides of the cell (Cell5) to encode the two messages. The left uses a solid isosceles triangle, whose apex is along the opposite direction of the time axis, to represent the occurrence of a rising edge and the signal’s disappearing state when entering the slice. The right uses another solid isosceles triangle, whose apex is along the direction of the time axis, to represent the occurrence of a falling edge and the signal’s disappearing state when leaving the slice. We divide the cell (Cell5) into two groups to represent multiple CSCPs occurring in a slice (e.g., Cells 7–10 in Fig. 4(b)).

This visual encoding method has many advantages. First, the combination of a triangle and rectangle ensures the consistency of communication states of adjacent slices (e.g., Cells 3, 4, and 5 in Fig. 5(a)). Second, isosceles triangles have good visual saliency and stability because angles and blank areas in a cell are visually notable, and the two legs of an angle have the same length. Third, triangles have good semantic clarity because the apex direction of a triangle reflects a CSCP’s type (e.g., a rising edge in Cell3 or a falling edge in Cell5 in Fig. 5(a)), and the apex directions of two triangles in the same cell indicate the occurrence of a single short communication (e.g., Cell1 in Fig. 5(a)) or a single short discontinuity (e.g., Cell6 in Fig. 4(b)) in a slice. Lastly, the frequent occurrences of multiple short communications or short discontinuities in a slice are visually encoded by an umbrella-triangle without a moiré effect (e.g., Cells 6 and 10 in Fig. 5(a)).

Before arriving at this design, we discussed many alternatives with our target users. For example, using an aggregated TF diagram (e.g., Fig. 2(c) and Fig. 5(b)). We also tried replacing a triangle with a semicircle (Fig. 5(c)); however, the visual stability of semicircles was worse than that of triangles, which could affect viewers’ estimation of CSCP locations on the time axis. We also modified VERule2 to use one triangle in one cell only. This generated two kinds of triangles with different sizes and angles, which could confuse viewers (e.g., Cells 1 and 3 in Fig. 5(d)). Alternative designs that represented multiple CSCPs occurring in a slice were tested. As two alternatives shown in Fig. 5(e–f), the former caused a moiré effect [10, 57], while the latter was easily confused with the design of the anomaly visualization.

### 5.3 Signal Anomaly Visualization

To highlight the four types of anomalies (R3), the ASTF diagram supports two visual cues that can be added to a cell. A short red line along the time direction at the center of a cell represents the existence of frequency or/and bandwidth anomalies (Fig. 3(h)). A short red line along the frequency axis direction at the center of a cell represents the existence of strength or/and SNR anomalies. For example, in the first cell of Signal-02 in Fig. 3(h), a vertical red line represents that frequency or/and bandwidth anomalies occur in the corresponding slice; in the first cell of Signal-01 in Fig. 3(h), vertical and horizontal red lines represent the possible co-occurrence of four types of anomalies.

These visual cues are simple and visually orthogonal to prevent visual interference with each other. The four types of anomalies are grouped to reduce the complexity of visual cues. Empirically, frequency and bandwidth anomalies often co-occur, like the co-occurrence of strength and SNR anomalies. Our users prefer a red line along the time axis to represent frequency or/and bandwidth anomalies (R4).
6 TIME SEGMENTATION ALGORITHM

To segment a binary communication state sequence into time slices while fulfilling an optimization goal, a new time segmentation algorithm is proposed. The resulting slices are applied to generate an abstracted time visualization (Section 5.2). This section details the optimization goal definition and the new algorithm.

6.1 Optimization Goal Definition

Time segmentation is an optimization problem that depends on a predefined optimization goal. The CSCP distribution in a binary sequence is the main information of interest to users, and the time segmentation is executed in data space while the result is visually encoded in visual space. Therefore, the optimization goal is to minimize the information loss of CSCP distribution during the segmentation and visual encoding to ensure that the visual CSCP distribution in visual space is similar to the actual CSCP distribution in data space. To measure the information loss, three quantified metrics are designed by considering the inner relationships between two spaces.

(1) The similarity of CSCP distributions (Sim_CD)

Sim_CD measures the similarity of CSCP distributions between data and visual spaces. Its calculation needs to obtain the exact location of each CSCP on the time axis. However, in visual space, because CSCPs have been encoded by isosceles triangles, there are no exact locations. We solve this problem from both spaces.

In visual space, we stipulate that the point of projecting the midpoints of the legs of an isosceles triangle onto the time axis is the visual location of CSCP(s), regardless of whether this triangle represents one or multiple CSCPs. For example, the visual CSCP location represented by the triangle in Cell1 (Fig. 6(a)) is at 2.5 seconds. This stipulation adopts the principle of area equivalence to estimate a visual CSCP location because area perception is familiar to users and a rectangle that has the same area as an isosceles triangle is easy to find (Fig. 6(b)). Thus, given

\[
Sim_{CD} = \sum_{i=1}^{m} \left| \frac{D_i}{T} - \frac{V_i}{L} \right|
\]

where \(m\) is the number of CSCP location pairs, \(V_i\) is the \(i\)th visual CSCP location in visual space and \(D_i\) is the corresponding exact or aggregated CSCP location in data space, \(T\) is the entire time span of data space, and \(L\) is the entire length of the time axis in visual space. A value approaching 0 indicates a “perfect” result.

(2) The difference in duty ratios (Dif_DR)

A duty ratio is the proportion of time during which a radio signal is appearing. The visual duty ratio of a signal in visual space may differ from the actual duty ratio in data space. Sim_CD cannot precisely reflect such differences due to the usage of aggregated CSCP locations. In Fig. 7(a), the visual duty ratio of the signal in Cells 3 and 4 seems large, but the actual duty ratio in Slices 3 and 4 is small. Thus, Dif_DR is defined to measure such differences.

The actual duty ratio of a signal can be calculated directly in data space, while the visual duty ratio cannot be directly calculated in visual space. To solve this problem, we thus use the area equivalence principle (Fig. 6(b)) to obtain the visual duty ratios of 10 classes of CSCP distributions in visual space. That is, the ratio of the colored area to the entire area in a cell is used to represent the visual duty ratio of the cell (Fig. 6(c)). Thus, given \(n\) slices and \(n\) cells, Dif_DR is formulated as:

\[
Dif_{DR} = \left| \text{actual}_{DR} - \frac{1}{n} \sum_{i=1}^{n} \text{visual}_{DR_i} \right|
\]

where \(\text{actual}_{DR}\) represents the actual duty ratio of a signal in data space, which is calculated using the number of logic “1”s divided by the entire time span \(T\); and \(\text{visual}_{DR_i}\), which is the visual duty ratio of the \(i\)th cell. A value approaching 0 indicates a “perfect” result.

(3) The coefficient of variation of time spans of slices (CV_TS)

In visual design, the size of each cell on the time axis is equal in visual space. If slices in data space have largely differentiated time spans, the visual CSCP distribution and duty ratio presented in visual space may be distorted. Therefore, CV_TS is defined to measure the dispersion of slices’ time spans. The coefficient of variation is used instead of standard deviation for the calculation because the means of the time spans of the slices in two segmentation results may be different.
Given $n$ slices, $\text{CV}_{\text{TS}}$ is formulated as:

$$\text{CV}_{\text{TS}} = \sqrt{\frac{1}{n} \sum_{i=1}^{n} (t_i - \bar{t})^2},$$

where $t_i$ represents the time span of the $i$th slice, and $\bar{t}$ represents the mean of time spans of all slices. A small value indicates a good result.

(4) Loss function design based on the above three metrics

Using the three metrics, the loss function is defined as:

$$\min_{x} F(x) = w_1 \cdot \text{Sim}_{\text{CD}} + w_2 \cdot \text{Dif}_{\text{DR}} + w_3 \cdot \text{CV}_{\text{TS}},$$

where $w_1$, $w_2$, $w_3 \in [0, 1]$ and $\sum_{i=1}^{3} w_i = 1$.

6.2 Algorithm Design

To segment a binary sequence of communication states of a signal into time slices, a new time segmentation algorithm, i.e., BSSVA, is designed by making use of a two-strategy and two-stage optimization. Although five time segmentation strategies existed (Section 2.3), no single strategy achieved satisfactory segmentation results in our pilot tests. Interestingly, combining the FP and EL strategies showed potential for two reasons. First, CSCPs are natural feature points for applying FP, but FP has a high time cost and cannot control for the dispersion of time spans of slices. Second, EL can rapidly divide a sequence into slices with equal time spans but ignores CSCPs. Moreover, a satisfactory segmentation result relies on identifying two keys, namely, an optimal number of segments $n$ and $n$-1 optimal dividing points. Our approach adopts a two-stage optimization to identify the two keys in two stages in accordance with the two-strategy combination idea.

STAGE I. Obtain an optimal $n$ using an EL strategy.

This stage uses an EL strategy to obtain an optimal $n$ and initial $n-1$ dividing points. Given a sequence and $n$ ranging from $N_{\text{min}}$ to $N_{\text{max}} (n \in n^2)$, $n$ is traversed from $N_{\text{min}}$ to $N_{\text{max}}$. On each traversal trial, the sequence is evenly divided by $n-1$ tentative dividing points. Notably, we need to move each tentative dividing point to the nearest integral position on the time axis if the entire period is not divisible by $n$ because the sequence has an interval of 1 second. After traversing, many groups of tentative dividing points are obtained. Each group can generate $n$ tentative slices in data space and $n$ tentative cells in visual space. We can thus calculate the loss of each group by using the loss function from Section 6.1. The group with the smallest loss contributes an optimal $n$ with $n-1$ initial dividing points for the next stage.

This stage takes minimal time to obtain an optimal $n$ because the time cost of EL is negligible in each traversal step and the range of $n$ is limited in [30, 50] from Section 5.2. This stage obtains initial slices with an equal time span, which is ideal for the CV_TS metric in the optimization goal. This stage also produces initial dividing points to reduce the searching space of optimal dividing points in the next stage.

STAGE II. Obtain optimal dividing points using an FP strategy.

If the initial dividing points are used to generate visualization, the actual CSCP distribution and duty ratio of a signal in data space may be distorted in visual space. Taking Slices 1–4 and Cells 1–4 in Fig. 7(a) as examples, a long distance exists between the falling edge in Slice2 and the rising edge in Slice3, but the distance is perceived as short in Cells 2 and 3. The duty ratio in Slices 3 and 4 is small but perceived as large in Cells 3 and 4. To prevent such distortions, we need to adjust the locations of initial dividing points. Fig. 7(b) shows an adjustment result, in which the visual CSCP distribution and duty ratio in visual space are perceived as very close to the actual ones in data space.
Table 1. Results of the algorithm experiment. Bold indicates the best indicator value among the algorithms under the same data conditions.

| Indicator | Data | Complexity | BSSVA (Ours) | EL | SW | BU | TD | FP |
|----------|------|------------|--------------|----|----|----|----|----|
|          | Time Span |           |              |    |    |    |    |    |
| Avg loss | A week      | Moderate   | 0.064        | 0.076 | 0.071 | 0.143 | 0.139 | 0.488 |
|          | A month     | High       | 0.114        | 0.152 | 0.128 | 0.191 | 0.197 | 0.315 |
| Avg time (s) | A week      | Moderate   | 0.166        | 0.181 | 0.176 | 0.210 | 0.225 | 0.269 |
|          | A month     | High       | 0.176        | 0.188 | 0.185 | 0.247 | 0.258 | 0.270 |

In terms of average time, significant differences were found. EL performed significantly better than the other algorithms. SW and BSSVA had relatively small time costs, but TD and BU exhibited relatively large time costs because SW had a “one-pass” feature, BSSVA took a small number of iterations (less than the number of slices obtained by EL), while TD and BU required a large number of iterations. FP presented a moderate time performance since its number of iterations was mainly influenced by the number of CSCPs of a signal. Moreover, the influence of the increase in the number of CSCPs on the time costs was greater than that of the increase in the time spans.

7.2 User Study

A user study was conducted to evaluate the effectiveness of the proposed ASTF diagram in long-term radio signal analyses. The scrolling TF diagram (Fig. 2(b)) and aggregated TF diagram (Fig. 2(c)) were selected as references and named as Sc-TF and Ag-TF, respectively. Thirty participants were recruited to participate in the study (i.e., 9 females and 21 males, aged 19−25 years; median age: 21; normal or corrected-to-normal visions). They were graduate students majoring in communication engineering and familiar with using TF diagrams. The participants were evenly divided into three groups, and each group used one of the three diagrams. The user study was conducted on a desktop with a 23.8-inch 1920 × 1080 display.

During the study, the participants were asked to answer 18 objective questions that required specific information corresponding to one of the analytical requirements (R1−R3 in Section 3) by observing a diagram. For example, “How many radio signals can be found?”, “How many discontinuities does the signal occur?”, “Which of the following four descriptions can reflect the time-varying patterns of the signal?” and so on. Thirty-six datasets with different time spans (i.e., 1 day, 3 days, and 1 week) were prepared. The participants needed to complete two trials for each question with two datasets. After accomplishing their tasks, the participants were asked whether the examined diagram was useful. They rated their overall feelings by requirement using a five-point Likert scale ranging from 1 (strongly disagree) to 5 (strongly agree) and then provided any thoughts they had. The full list of objective questions is provided in the supplementary material.

![Fig. 8. Objective results of the user study in (a) mean accuracy and (b) mean completion time by requirement. Error bars indicate standard errors.](image-url)
The answer and completion time of each participant for each trial were recorded and the mean accuracy and mean time by requirement (Fig. 8) and question (see the supplementary material) were computed as metrics. Significance analyses with Friedman tests were conducted to examine the differences ($p < 0.05$) among the groups in the two metrics and three requirements.

In terms of accuracy (Fig. 8(a)), no significant differences were found between the Ag-TF and ASTF groups in R1 and R2. The Ag-TF group (91%) achieved an accuracy close to that of the ASTF group (92%) in R1, probably because Ag-TF and ASTF had the same basic layout that could explicitly present the number of signals and their basic characteristics. The Ag-TF group had a lower accuracy (80%) than the ASTF group (95%) in R2 because some short discontinuities were lost after being aggregated in Ag-TF. The Sc-TF group performed worst in R1 and R2, likely because Sc-TF cannot directly provide an overall picture, and the participants had to scroll to search for the acquired information. Significant differences were found in R3. The ASTF group significantly performed better than the other groups in R3. The Sc-TF group (36%) outperformed the Ag-TF group (28%) in R3, possibly because a few anomalies can be found by observing unprocessed raw spectrum data in Sc-TF, even though anomalies were not explicitly encoded in Sc-TF and Ag-TF.

In terms of time (Fig. 8(b)), the Sc-TF group took significantly longer to complete R1 − R3 due to inevitable scrolling operations when using Sc-TF. No significant differences were found between the ASTF and Ag-TF groups in R1 − R3. Most participants in the two groups completed a question in 20 seconds. Moreover, the ASTF group was slightly slower than the Ag-TF group in R1, probably because some participants were not familiar with the visual encodings in ASTF.

The subjective ratings of the participants are shown in Fig. 9. The rating medians are as follows. R1: Sc-TF ($m = 4$), Ag-TF ($m = 5$), and ASTF ($m = 4.5$); R2: Sc-TF ($m = 3$), Ag-TF ($m = 4$), and ASTF ($m = 4.5$); R3: Sc-TF ($m = 3$), Ag-TF ($m = 1$), and ASTF ($m = 4.5$). Ag-TF obtained the highest rating median in R1. Several participants commented, “Ag-TF’s visualization is simple and effective in presenting signal distribution and characteristics.” Sc-TF obtained the lowest rating medians in R1 and R2. Some participants stated, “It is exhausting to use Sc-TF. I have to scroll the diagram many times and some details are easily overlooked. Importantly, the previously noticed information is often forgotten after scrolling.” ASTF obtained the highest rating medians in R2 and R3. Participants made comments such as, “ASTF is informative and helpful in answering all questions”, “It seems that there are no anomalies in Ag-TF”, “Some short discontinuities in the ground truth cannot be seen in Ag-TF. Some short discontinuities are just light white lines, which are indistinguishable”, and “It would be great to connect a Sc-TF with an ASTF to form an overview-detail mode”.

8 DISCUSSION

8.1 Limitations

ASTF diagrams address the scalability of TF diagrams in terms of time but not frequency. The frequency range that can be utilized by human beings is extremely wide, but raw radio spectrum data generally have narrow bands limited by the spectrum sensing capability of mainstream equipment (e.g., 36 MHz or 72 MHz). Even so, wide-band spectrum data can be obtained through complicated post-processing. Therefore, the scalability for frequency is important and challenging.

ASTF diagrams may encounter three unique problems in practice. First, sparse and dense areas may co-exist in ASTF when signals are unevenly distributed on the frequency. This problem could be solved by providing interval adjustment functions or zooming interactions. Second, the height-width ratio of a cell in visual space could be small when representing a signal with a wide bandwidth. A potential solution could be to set a minimum height-width ratio of a cell in visual space. Lastly, the number of slices of multiple signals may be slightly different if segmenting solely on signals. Generally, such differences have little impact. Finding an optimal $n$ on all signals could avoid this problem.

The BSSVA algorithm has three limitations. First, the algorithm cannot be directly applied to streaming data due to its data pre-processing mode. A potential solution could be to adopt an incremental data processing mode [22, 52]. Second, the algorithm’s result may not be globally optimal. Two alternatives possibly achieve smaller losses than the algorithm. The one is to find an optimal $n$ in STAGE II instead of STAGE I. The other is to adopt a genetic algorithm for time segmentation [24, 28]. We tested these two alternatives in pilots and the results seemed to show that losses did not decline substantially but time costs increased greatly. Lastly, the time performance can be improved. A feasible solution is to introduce parallel computing techniques [40].

8.2 Implications

ASTF diagrams have the potential to become a common visual component in visual analysis systems for radio monitoring and management. An ASTF diagram could act as a superior view in a multi-viewed interface to provide an overview of the time-varying signals in a large time span. Users thus could select a short time span of interest in the ASTF diagram to update a TF diagram to observe details in raw radio spectrum data. Moreover, ASTF diagrams could provide semantic interactions on signals to fulfill advanced analysis tasks. For instance, when comparing the communication behaviors of two signals, users could select the two signals to filter out the other signals in an ASTF diagram and then juxtapose them closely in frequency to facilitate the comparison. Such interactions cannot be directly supported in TF diagrams because radio spectrum data are not formatted in structured signal records. See the supplementary material for demonstrations.

The visual abstraction method and the BSSVA time segmentation algorithm can be applied to visualize long-term binary sequences generated in various domains for time-varying pattern analyses. For example, a sensor that reports whether a car parking spot is or is not occupied at a certain frequency can produce long-term binary sequences. A monitor of digit circuits can also produce long-term binary sequences. Moreover, common time series data can be converted into binary sequences by setting appropriate thresholds on-demand.

9 CONCLUSION

This paper presents a new visual diagram, ASTF, that can depict the time-varying patterns of radio signals to fulfill long-term signal analysis requirements. A visual abstraction method and a time segmentation algorithm are proposed to assist in implementing the new diagram. The new diagram can be combined with a traditional TF diagram to work in a hierarchical way in a visual analysis system for radio signal analyses. The new diagram can also provide semantic interactions on signals in the system to facilitate advanced signal analysis tasks. The proposed visual abstraction method and time segmentation algorithm can be applied for the visualization of other binary sequences.

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