Zhang, Liang and He, Wenlong and Clarke, Jim and Ronald, Kevin and Phelps, Alan D. R. and Cross, Adrian (2019) Systematic study of a corrugated waveguide as a microwave undulator. Journal of Synchrotron Radiation, 26 (1). pp. 11-17. ISSN 1600-5775 , http://dx.doi.org/10.1107/S1600577518014297

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Systematic study of a corrugated waveguide as a microwave undulator

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Microwave undulators have great potential to be used in short-wavelength free-electron lasers. In this paper, the properties of a corrugated waveguide and its performance as an undulator cavity for a UK X-ray free-electron laser were systematically studied. The equations presented in this paper allow a fast estimation of the dimensions of the corrugated waveguide. An undulator cavity operating at 36 GHz designed for the HE_{11} and HE_{12} modes was investigated and the performance of both modes compared.

1. Introduction

Undulators are one of the most important components in a free-electron laser (FEL) (Deacon et al., 1977; Huang & Kim, 2007). Currently, the conventional permanent magnet undulator (PMU) plays the dominant role. Microwave undulators (MUs) (Shintake et al., 1982, 1983) that also have a periodic magnetic field can be potential undulators and have the following advantages. (i) Fast dynamic control of the polarization (Shumail & Tantawi, 2016). (ii) Easy control of the field strength, which can be adjusted through the input microwave power, whereas, in a PMU, mechanical methods to adjust the magnet gap or the magnet period have to be used which can be complicated. (iii) It is challenging for a PMU to achieve short periods as the magnetic field strength would be significantly reduced. In contrast, for an MU the equivalent period is mainly determined by the wavelength of the electromagnetic wave, therefore a short period can be achieved if the MU operates at a higher frequency. (iv) The MU is essentially a metallic cavity and hence it is robust against damage by ionizing radiation near electron beam dump regions, as compared with the PMUs that are made of rare-earth materials, which may be more susceptible to damage in harsh ionizing radiation environments.

However, since the concept of the microwave undulator was proposed in 1982 (Shintake et al., 1982), progress has taken longer than expected, mainly due to the limited availability of high-power microwave sources. In 1983 (Shintake et al., 1983), the first MU experiment was carried out and an equivalent magnetic field $B_u$ of 0.045 T with an undulator parameter $K$ of 0.24 was achieved when driven by a 300 kW, 2.856 GHz microwave source. A ridged rectangular cavity was used and a quality factor $Q$ of 7100 was measured. To achieve a similar performance to a state-of-the-art PMU, for example, 1.29 T for a 15 mm-period PMU used in the Swiss-FEL at the Paul Scherrer Institute, the required driving power would need to be more than 20 MW at 10.5 GHz (assuming the same $Q$ factor.
of 7100 can be achieved for a similar structure scaled for operation at 10.5 GHz. However, the electric field at the wall of the ridged rectangular cavity would be too high and susceptible to microwave breakdown. A significant improvement on the MU was made with the use of a low-loss HE$_{11}$ mode in a corrugated waveguide. A cavity made of a corrugated waveguide operating at the X-band was measured and it was able to achieve a $Q$ factor as high as 91 000. When it was driven by a 50 MW SLAC klystron at 11.424 GHz (Tantawi et al., 2014), such an MU was able to achieve an equivalent $B_u$ of 0.65 T with a period of 13.9 mm.

The corrugated waveguide is normally overdamped. The numerical calculation of the eigenmodes of the cavity made with the corrugated waveguide is time-consuming. In this paper, analytical equations and design constraints are summarized which could be used to quickly estimate the dimensions of the structure. The microwave undulator can be operated at a high millimetre-wave frequency to achieve a smaller period. In this paper, a corrugated waveguide operating at 36 GHz was designed as an MU for a UK XFEL.

The paper is organized as follows. In Section 2, the principle of the MU and the relation between the cavity and the microwave sources is presented. Section 3 introduces the theory of the corrugated waveguide and the equations that determine the dimensions, field distribution and the loss coefficient. Section 4 details the simulation results of an MU operating at 36 GHz. Both the HE$_{11}$ and HE$_{12}$ operating modes were investigated and their performances compared.

2. Principles of MU

The principle of the MU can be found in the literature (Pellegrini, 2006; Seidel, 2001; Shintake et al., 1983; Shumail & Tantawi, 2016). The relativistic electrons in an MU cavity will interact with both the electric field $E_x = E_0 \sin(2\pi z/\lambda_e) \sin(\omega t)$ and magnetic field $B_y = B_0 \cos(2\pi z/\lambda_e) \cos(\omega t)$. Compared with a PMU, the Lorentz force in an MU can be rewritten in the form

$$F_x = \frac{eE_0}{2} \left( \frac{\zeta}{Z_w} + 1 \right) \cos \left[ 2\pi z \left( \frac{1}{\lambda_0} + \frac{1}{\lambda_b} \right) \right]$$

$$+ \frac{eE_0}{2} \left( \frac{\zeta}{Z_w} - 1 \right) \cos \left[ 2\pi z \left( \frac{1}{\lambda_0} - \frac{1}{\lambda_b} \right) \right],$$

where $e$ is the charge on the electron, $\lambda_0$ is the free space wavelength, and $\lambda_b$ is the wavelength of the electromagnetic wave in the undulator cavity. $E_0$ and $B_0$ are the peak electric and magnetic field strength in the microwave undulator cavity, respectively. $Z_w$ is the wave impedance in the cavity and $\zeta$ is the wave impedance in free space. The second term leads to a long wavelength and is undesirable in the undulator of a short-wavelength FEL. The second term can be ignored if the wave impedance is close to the free-space impedance, which means the operating frequency is far from the cut-off frequency of the waveguide. In this case, the equivalent magnetic field $B_u$ and wavelength $\lambda_u$ of the microwave undulator are given by

$$B_u = \frac{E_0}{2\zeta} \left( \frac{\zeta}{Z_w} + 1 \right),$$

$$\frac{1}{\lambda_u} = \frac{1}{\lambda_0} + \frac{1}{\lambda_b}.$$  \hfill (2)

If the microwave source starts to fill the cavity at time zero, the stored energy at time $t$ in the cavity can be expressed as (Alvarez, 1986)

$$W(t) = P_0 \tau_0 \frac{4\beta}{(1 + \beta)} \left[ 1 - \exp \left( - \frac{1 + \beta}{2} \frac{t}{\tau_0} \right) \right]^2,$$  \hfill (3)

where $P_0$ is the input power, $\tau_0 = Q_0/\omega$, and $\beta = Q_0/Q_e$. $Q_0$ and $Q_e$ represent the intrinsic and external quality factor of the cavity. In a steady state, where $t \gg \tau_0$, the stored energy reaches its maximum value of $P_0\tau_0$ if the coupling aperture is specifically designed to achieve $\beta = 1$. The input power in this case will be equal to the Ohmic loss in the cavity. In the cases of an under-coupled ($\beta < 1$) and over-coupled ($\beta > 1$) regime, the stored energy in the steady state is smaller. The filling time of the cavity $\tau_0$ can be calculated if a charging factor $Q_e$, defined as the ratio of the charged energy and its maximum value, is known.

$$\tau_0 = \frac{Q_0}{\omega} \frac{2}{1 + \beta} \ln \left( \frac{1 + \eta^{1/2}}{1 - \eta} \right).$$  \hfill (4)

From equations (3) and (4), to achieve maximum storage at a given input power, a higher $Q$ factor of the cavity is preferred; however, the filling time increases simultaneously. In applications of MUs, high-power microwave sources with output powers of megawatts or more are needed to achieve a high equivalent magnetic field. Such high-power microwave sources normally operate in pulsed mode to reduce the power supply requirements and associated thermal stress. The filling time of the MU cavity should match the pulse length of the microwave source. The coupler can be slightly over-coupled to reduce the filling time while maintaining a high $Q$ factor. If the input microwave frequency is 36 GHz, with a 2 μs pulse length, the $Q$ factor of the cavity should be under 150 000 if $\beta = 1$ and $\eta = 0.9$.

The electric field strength inside the cavity along the electron beam path can be calculated by careful selection of the operating mode of the cavity. Knowing the input power and $Q$ factor, the parameters of the MU can be determined.

3. Corrugated waveguide

A high-$Q$ low-loss cavity is of great importance when it is used as an MU. In a circular waveguide, the mode with the lowest loss is the TE$_{01}$ mode. However, the field strength at the waveguide center for this mode is small and hence is not a good option for an MU as the electrons are to propagate down the center of the structure. A corrugated waveguide, as shown in Fig. 1, can be used in other applications such as a feed horn for a transmission line system due to its advantages of low cross-polarization field, low loss and wide bandwidth. Its low attenuation feature is attractive for the transmission of high-
power microwaves. The fundamental mode HE_{11} was found to have lower loss compared with the TE_{01} mode in the circular waveguide. It has been used to transport megawatt-level millimetre-wavelength radiation generated by gyrotron oscillators for fusion experiments such as ITER. In recent years, the corrugated waveguide has been proposed as an MU (Shumail et al., 2011; Chang et al., 2012; Toufexis & Tantawi, 2016). The corrugated waveguide can be shortened at both ends to form a cavity. The resonance frequency of the corrugated waveguide with the linearly polarized mode sets can be simplified as (Claricoats & Saha, 1971)

$$E_z = a_n J_n(Kr) \cos(m \varphi),$$
$$E_i = -j a_n (k/K) J_{m \mp 1}(Kr) \cos(m \varphi),$$
$$E_\varphi = \mp (-j) a_n (k/K) J_{m \mp 1}(Kr) \sin(m \varphi).$$

Usually, a higher order HE or EH mode is not linearly polarized. The suitable operating modes in the corrugated waveguide for the microwave undulator application are the HE_{11} and HE_{12} modes because they are low loss, linearly polarized and have the peak electric field at the waveguide center. The electric field patterns of the HE_{11} and HE_{12} modes are shown in Fig. 2. The HE_{12} mode has larger field density at the waveguide center. It can have a bigger electric field compared with the HE_{11} mode at the same input power.

The attenuation coefficient defined by the ratio between the lost power and the transported power per meter for the HE_{1n} modes, under the balanced hybrid condition, can be written as (Claricoats & Olver, 1984; Doane, 1985)

$$\alpha = \frac{1}{2} \frac{R_e}{Z_0} \frac{\pi}{\lambda_0} \left[ \frac{1}{x_t^2 k^2} \left( 1 + \frac{x_t \pi}{2} \right) + \frac{x_t}{x_t^2} \right],$$

where $Z_0 = 1/\gamma_0$ is the free space wave impedance, $R_e = (\pi f \mu_0 \sigma)^{1/2}$ is the resistivity of the corrugated metal waveguide and $\sigma$ is the conductivity of the metal. In this paper, oxygen-free high-conductivity copper was chosen and $\sigma = 5.8 \times 10^7$ S m$^{-1}$ was used in the simulation. Equation (9) implies that the attenuation coefficient is proportional to $r_t^{-3}$ and $f^{-2}$ in the case of $x_t^2 \gg 1$.

The corrugated waveguide can be shortened at both ends to form a cavity. The resonance frequency of the corrugated waveguide can be estimated as

$$f = \frac{c}{\lambda_0} = \frac{c}{2 \pi} \sqrt{K^2 + \left( \frac{N \pi}{\lambda_0} \right)^2} \frac{1}{2^{1/2}},$$

where $c$ is the speed of light, $N$ is an integer and $\lambda_0$ is the wavelength of the resonance mode in the cavity. Because the
A corrugated waveguide as a microwave undulator

4. Design of a corrugated waveguide for an MU

A corrugated waveguide cavity operating at 36 GHz was designed as a potential microwave undulator for the UK XFEL. The initial geometry parameters were calculated from the equations described in previous sections. Both of the HE$_{11}$ and HE$_{12}$ modes are considered. A summary of the geometry parameters as well as the undulator deflection parameter $K_u = 0.09336B_u\lambda_0$ [T mm] are listed in Table 1.

The accurate resonance frequency and $Q$ factor of the designed structure were simulated using CST Microwave Studio. The simulated structure was set at six corrugation periods to significantly reduce the simulation time. For such a short cavity length, the loss at the conducting wall at both sides will be much larger than the loss at the corrugated wall because the field strength at the corrugated wall is much smaller. In the simulation, a periodic boundary condition was set at both ends of the corrugated waveguide. In this way, the desired. Therefore $r_1$ should be as small as possible under the constraint of $kr_1 \gg 1$. On the other hand, it is preferred for the electron beam that travels through the microwave undulator to see a uniform field in the radial direction. The minimum waveguide radius can be solved from the field pattern of the operating mode if the electron beam aperture $R_b$ and a threshold, for example 90% of the maximum field at the beam edge, are defined. For HE$_{1n}$ modes, it follows that $J_1(KR_b) = 0.9$. Taking the first two solutions of $J_0(Kr_1) = 0$, $K$ is approximately equal to 2.4$/r_1$ or 5.5$/r_1$ for the HE$_{11}$ or the HE$_{12}$ mode, respectively. Therefore the following parameters were chosen,

$$r_1 = \begin{cases} 3.8R_b, & \text{for the } HE_{11} \text{ mode}, \\ 8.6R_b, & \text{for the } HE_{12} \text{ mode}, \\ \end{cases}$$

resulting in a reasonable value of $r_1$. Meanwhile the value of $r_1$ should satisfy $x_1^* = 2\pi r_1/\lambda_0 \gg 1$. If $x_1^* = 5$ is used, then $r_1 \geq 0.8\lambda_0$ and the results become

$$r_1 = \begin{cases} \text{maxima}(3.8R_b, 0.8\lambda_0), & \text{for the } HE_{11} \text{ mode}, \\ \text{maxima}(8.6R_b, 0.8\lambda_0), & \text{for the } HE_{12} \text{ mode}. \\ \end{cases}$$

Table 1

| Operating mode | HE$_{11}$ | HE$_{12}$ |
|----------------|----------|----------|
| Operating frequency (GHz) | 36 | 36 |
| $\lambda_0$ (mm) | 8.33 | 8.33 |
| $R_b$ (mm) | 2.0 | 2.0 |
| $r_1$ (mm) | 4.8$R_b = 8.0$ | 9.6$R_b = 18.0$ |
| $d = \lambda_0/4$ (mm) | 2.1 | 2.1 |
| $\lambda_x$ (mm) | 9.06 | 9.12 |
| $p = \lambda_0/3$ (mm) | 3.00 | 3.02 |
| $w$ (mm) | 0.5 | 0.5 |
| $b = p - w$ (mm) | 2.50 | 2.52 |
| $Q$ factor | 94344 | 187073 |
| Input power (MW) | 50 | 50 |
| Peak $E_x$ on axis (V m$^{-1}$) | $3.8 \times 10^8$ | $3.7 \times 10^8$ |
| $B_u$ (T) | 1.27 | 1.23 |
| $\lambda_u$ (mm) | 4.34 | 4.35 |
| $K_u$ | 0.52 | 0.50 |

4. Design of a corrugated waveguide for an MU

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corrugated waveguide is normally overmoded, $\lambda_0 \simeq \lambda_x$ when $N = 2$. As mentioned earlier, the surface-impedance approach gives a good approximation when $\lambda_0/p$ is a reasonably large value. Therefore, when designing the corrugated waveguide, the period $p$ can be selected to be smaller than $\lambda_0/2$. It is of course the case that ‘the smaller the period, the better’; however, as the operating frequency increases, the wavelength becomes smaller, resulting in a small corrugation period and a thin corrugation slot of $w \simeq 0$ which significantly increases the machining difficulty. The final choice of the geometry should therefore also consider the machining tolerance.

Since $x_1^* = kr_1 = 2\pi r_1/\lambda_0 \gg 1$ has to be satisfied, the corrugated waveguide radius $r_1$ is a large value. As the attenuation coefficient is proportional to $r_1^{-1}$, it is preferable to have a large $r_1$ at a given operating frequency. From equation (8), the waveguide radius affects the field strength if the input power is a fixed value. In a microwave undulator, a high field at the electron beam path, in this case the waveguide center, is
loss at both sides will not be included. Fig. 3 shows the electric field distribution of the cavity modes of HE\(_{11}\) and HE\(_{12}\). The peak \(E_x\) field along the \(z\) axis was obtained from the field distribution of the eigenmode and normalized to an Ohmic loss power of 50 MW at a cavity length of 1 m. With the same input power and similar operating frequency, the waveguide radius of the HE\(_{12}\) mode was about 2.2 times that of the HE\(_{11}\) mode, and its \(Q\) factor was nearly 2 times that of the HE\(_{11}\) mode. The \(E_x\) field strength was slightly smaller than that of the HE\(_{11}\) mode. The equivalent magnetic field \(B_u\) was also similar for both cases.

Parameter scans were used to study the effects of varying of the corrugation geometry parameters such as the corrugation period \((p)\), the slot length \((w)\) and the waveguide radius \((r_1)\). The results of resonance frequency, \(Q\) factor and equivalent magnetic field strength are shown in Figs. 4–6. The HE\(_{11}\) mode has a similar trend to the HE\(_{12}\) mode. In Fig. 4, as the corrugation period increases, the resonance frequency becomes smaller while the slot length \((w)\) and the waveguide radius \((r_1)\) are kept the same. The results matched the theoretical calculation well from equation (10) and the scaling law equations (Shumail et al., 2011). The difference between the simulation and theoretical calculation is less than 2%, therefore it allows a fast prediction of the cavity parameters from the theoretical analysis. The \(Q\) factor reduces as the corrugation period increases. It is mainly caused by the increase of the overall waveguide length and the decreases in the stored energy per unit length.

The simulation results at the different waveguide radii are shown in Fig. 5. The trends for the HE\(_{11}\) and HE\(_{12}\) modes are very similar. Increasing the waveguide radius would significantly increase the \(Q\) factor and the resonance frequency drops quickly. However, from equation (4), a high \(Q\) factor would result in a long filling time. For the HE\(_{11}\) mode, a 20% increment of the waveguide radius would lead to a \(Q\) factor close to 150 000, requiring an increase in the pulse length of the high-power microwave source used to drive the structure. Also, increasing the waveguide radius did not improve the equivalent magnetic field, which was almost the same. Therefore, the designed waveguide radius was considered to be optimal.

The simulation results of the variation in slot length while keeping the corrugation period constant are shown in Fig. 6. Only the CST simulation results were included as the theoretical analysis will not be accurate at small slot length values. As the slot length increases, the assumption of only the lowest TM standing wave appearing in the slot is no longer satisfied. The field at the corrugation wall became larger and caused a significant reduction in the cavity \(Q\). The \(Q\) factor dropped more quickly for the HE\(_{11}\) mode than the HE\(_{12}\) mode because its waveguide radius was smaller. As the corrugation period was kept constant, the change in the resonance frequency was small. The equivalent magnetic field \(B_u\) also changed by a small amount. The simulation results proved that the slot length should be as small as possible to achieve a high \(Q\)
factor. However, the difficulty in manufacturing such a structure while maintaining sufficient mechanical strength needs to be taken into account. A slot length of 0.5 mm is a reasonable value to satisfy the criteria of ease of manufacture, while at the same time being mechanically strong.

5. Discussion and conclusions

In this paper, a corrugated waveguide was studied as a microwave undulator for a UK XFEL. The equations that govern the performance of the microwave undulator are presented and have been used to estimate the dimensions of the corrugated waveguide.

Both of the HE\textsubscript{11} and HE\textsubscript{12} modes existing in the corrugated waveguide are suitable operating modes. Their characteristics were studied using numerical simulation and their performance compared in the design of a corrugated waveguide operating at 36 GHz. It was found that the equivalent magnetic field for both of the modes was very similar. The HE\textsubscript{12} mode had a much larger waveguide radius, which could be advantageous for high-frequency operation because it helps to reduce the difficulty in manufacture as well as reducing the electric field at the wall. The HE\textsubscript{12} mode is also less sensitive to the slot length compared with the HE\textsubscript{11} mode. The drawback of the HE\textsubscript{12} mode includes a much higher $Q$ factor that leads to a longer filling time and greater sensitivity to the waveguide period.

Funding information

The authors would like to thank the Science and Technology Facilities Council (STFC) UK and the Cockcroft Institute (Core Grant ST/P002056/1) for supporting this work.

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