The isospin structure of photoproduction of $\pi\eta$ pairs from the nucleon in the threshold region

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Abstract

Photoproduction of $\pi\eta$-pairs from nucleons has been investigated from threshold up to incident photon energies of $\approx 1.4$ GeV. The quasi-free reactions $\gamma p \rightarrow p\pi^0\eta$, $\gamma n \rightarrow n\pi^0\eta$, $\gamma p \rightarrow \pi^+\eta$, and $\gamma n \rightarrow p\pi^-\eta$ were for the first time measured from nucleons bound in the deuteron. The corresponding reactions from a free-proton target were also studied to investigate final-state interaction effects (for neutral pions the free-proton results could be compared to previous measurements; the $\gamma p \rightarrow n\pi^+\eta$ reaction was measured for the first time). For the $\pi^0\eta$ final state coherent production via the $\gamma d \rightarrow \pi^0\eta$ reaction was also investigated. The experiments were performed at the tagged photon beam of the Mainz MAMI accelerator using an almost 4r coverage electromagnetic calorimeter composed of the Crystal Ball and TAPS detectors. The total cross sections for the four different final states obey the relation $\sigma(\pi^0\eta) \approx 2\sigma(n\pi^0\eta) \approx 2\sigma(p\pi^-\eta) \approx 2\sigma(n\pi^+\eta)$ as expected for a dominant contribution from a $\Delta^+ \rightarrow \eta\Delta(1232) \rightarrow \pi\eta N$ reaction chain, which is also supported by the shapes of the invariant-mass distributions of nucleon-meson and $\pi$-$\eta$ pairs. The experimental results are compared to the predictions from an isobar reaction model.
1. Introduction

Photoproduction of mesons is a well established tool for the investigation of excited states of the nucleon. Reactions with meson pairs in the final state have gained a lot of interest because they allow the study of resonances that have small decay branching ratios to the nucleon ground state and decay instead via intermediate excited states.

The best studied double-meson final state is pion pairs. In particular, double $\pi^0$ production has been studied (see e.g. [1–6]). This reaction has the advantage that due to the small coupling of photons to neutral pions non-resonant background contributions are small. However, recently the $\pi\eta$ final state has also attracted interest. Total cross sections, invariant mass distributions, and also some polarization observables have been measured for the $\gamma p \to \pi^0\eta$ reaction at LNS in Sendai, Japan [7], GRAAL at ESRF in Grenoble, France [8], ELSA in Bonn, Germany [9–13], and at MAMI in Mainz, Germany [14,15] (see [16] for a recent summary). This decay channel is more selective than double-$\pi^0$ production. The $\eta$-meson is isoscalar, such that nucleon resonances can only emit it in $N^* \to N(\pi^0)$ or $\Delta^* \to \Delta(\pi^0)$ transitions. Thus, one expects that two classes of nucleon resonances are important for this reaction: excited $\Delta^*$-states with significant $\eta$-decays to the $\Delta(1232)$ and $N^*$ resonances decaying to $N(1535)$ in $1/2^-$ via pion emission. The main signature of the first decay type are pion - nucleon invariant masses peaking at the $\Delta(1232)$ mass, while the latter will produce $\eta$ - nucleon invariant masses close to the $N(1535)$ $1/2^-$ position. These two components have been identified in the previously measured invariant mass distributions, which in addition show a signal from the $a_0(980) \to \pi\eta$ decay in the $\eta - \pi$ invariant mass [9,10,13].

These analyses discovered a strong dominance of the $\Delta(1535)$ in the $1/2^-$ state, which is the predominant decay channel in the threshold region from the $\Delta(1700)/3^-/2^-$ and at higher incident photon energies from the $\Delta(1490)/3^-/2^-$ [10,14,17]. So far, there were only two cases where a photon-induced meson-production reaction is completely dominated by a single resonance and allows its almost background free study: pion production in the range of the $\Delta$ resonance and $\eta$ production via the $N(1535)$ in $1/2^-$ resonance [18,19]. Photoproduction of $\pi\eta$-pairs offers the same chance for the investigation of excited states of the nucleon. Reactions

The present paper summarizes the results from the measurement of quasi-free production of $\pi\eta$ pairs from nucleons bound in the deuteron for all four possible isospin combinations from Eq. 1 up to incident photon energies of 1.4 GeV. Total cross sections have been extracted for all four reaction channels and are compared to the results from the reaction model discussed in [14]. In addition, the total cross section for the coherent reaction $\gamma d \to d\pi^0\eta$ has been determined and compared to the model results from Egorov and Fix [22].
2. Experiment and Analysis

The experiment was carried out at the Mainz MAMI accelerator [32,33] using a quasi-monochromatic photon beam with energies up to ≈1.4 GeV from the Glasgow tagged photon spectrometer [34–36]. The primary electron beam (energy of 1.508 GeV, for some part of the beam time 1.577 MeV see [28]) produced bremsstrahlung photons in a copper radiator of 10 μm thickness. The energy resolution of the photon beam is related to the 4 MeV bin width of the tagger focal plane detectors.

Three different beam times with liquid deuterium targets and one measurement with a liquid hydrogen target for control were analyzed for the results summarized in this work. The same data set has already been analyzed in [6,28] for beam-helicity asymmetries in quasi-free photoproduction of $\pi^0\pi^0$ and $\pi^0\pi^\pm$ pairs, for total cross sections and angular distributions in single η production [29] and single $\pi^0$ production [30]. Details for the setup, target and beam parameters, and analysis procedures are discussed in these references. Here, only a short summary is given.

The detector setup (see [28,29] for schematic drawings and details) combined the Crystal Ball (CB) [38] and TAPS [39,40] electromagnetic calorimeters (CB: 672 NaI(Tl) crystals, TAPS: 384 BaF$_2$ crystals). The targets were mounted in the center of the CB and surrounded by a detector for charged particle identification (PID) [41]. For the same purpose, all TAPS modules had individual plastic scintillators in front of the crystals (‘TAPS-Veto’). The combined setup covered ≈ 97% of the full solid angle and detected photons from the decays of the neutral mesons, charged pions, protons, neutrons, and deuterons.

The analysis for the quasi-free reactions was almost identical to that for the $\pi^0\pi^0$ and $\pi^0\pi^\pm$ final states discussed in [6] and in [28]. In the first step, hits in both calorimeters were classified as ‘charged’ or ‘neutral’ depending on the response of the PID and the TAPS-Veto. Charged hits in CB were separated into protons and charged pions using the $\Delta E - E$ analysis of the PID and CB. The result is shown in Fig. 1. No direct separation between photons and neutrons was possible for hits in the CB. Neutral hits in the CB were therefore, in this stage of the analysis, accepted as candidates for photons and neutrons.

For hits in TAPS, photons and neutrons were separated as in [6,28,29] using a pulse-shape analysis (PSA) for the BaF$_2$ signals and a time-of-flight (ToF) versus energy analysis. Protons in TAPS were also required to have passed the PSA as nucleons, and the ToF-versus-E as protons. Recoil deuterons in TAPS were separated (for events with a $\pi^0\eta$ pair) from protons in the ToF-versus-E spectra, where they appeared as a clearly separated band. Charged pions in TAPS were not included in the analysis because the only identification possibility would have been ToF-versus-E, but protons (partly from reactions with much higher cross sections) that leaked into the pion band produced substantial background. This means that for the $\pi^+\eta$ and $\pi^-\eta$ final states, a small part of the total reaction phase space (charged pions at laboratory polar angles less than 20°) was not in the acceptance of the detector.

Seven different event classes were analyzed in total (see Table 1). They correspond to both types of pions ($\pi^0$ and $\pi^\pm$), to reactions with coincident recoil protons ($\sigma_p$) and coincident recoil neutrons ($\sigma_n$), the inclusive reaction $\sigma_{incl}$ without any condition for recoil nucleons, and for $\pi^0\eta$ in addition to the coherent reaction (coincident with recoil deuterons). The indices $p$ and $n$ refer to the final-state nucleons, protons and neutrons respectively. The inclusive reaction $\sigma_{incl}$ is independent from the recoil nucleon detection efficiencies and was used to check for systematic effects because it must satisfy the condition $\sigma_{incl} \approx \sigma_p + \sigma_n + (\sigma_d)$ ($\sigma_d$ contributes only for $\pi^0\eta$-pairs).

In the second step of the analysis, a $\chi^2$ test of the invariant masses of pairs of neutral hits was made for events with three and more neutral hits, testing the hypothesis of $\pi^0$ and $\eta$ invariant masses. The $\chi^2$ of all possible combinations of neutral hits to disjunct pairs was calculated from

$$\chi^2(k) = \sum_{i=1}^{n_m} \left( \frac{m_{i, \eta} - m_{i, k}}{\Delta m_{i, k}} \right)^2 \quad k = 1, \ldots, n_p,$$

where $n_m$ is the number of neutral mesons ($n_m = 1$ for $\pi^+\eta$ final states, $n_m = 2$ for $\pi^0\eta$) and $n_p$ is the number of different combinations of the neutral hits to pairs ($n_p = 1$ for 2n events, $n_p = 15$ for 5n events). The $m_{i, k}$ are the invariant masses of the i-th pair in the k-th permutation of the hits.
and the $\Delta m_{i,k}$ are the corresponding uncertainties computed event-by-event from the experimental energy and angular resolution. The mesons nominal masses $m_{\pi^0,\eta}$ were chosen such that for each event with four or five neutral hits, the hypotheses of a $\pi^0\eta$ and a $\pi^0\eta^0$ pair and for events with two or three neutral hits, the $\eta$ and $\pi^0$ hypotheses were tested. Only the combination with the minimum $\chi^2$ was selected for further analysis. For events with an odd number of neutral hits, for which no hit was directly identified as a neutron, the one which was not identified as a meson decay photon by the $\chi^2$-test was assigned to the neutron.

The two-dimensional invariant mass spectrum for the $\pi^0\eta$ final state is shown in Fig. 1. The regions around the $\pi^0\eta$ peaks are scaled up by a factor of 50 with respect to the $\pi^0\eta^0$ peak. The remaining background below the peaks appears mainly as a band at the $\pi^0$ invariant mass running parallel to the axis of $\eta$ invariant mass. The spectra were therefore projected onto $\eta$-invariant masses. They were fitted with a third degree polynomial and the simulated line shape of the $\eta$ invariant mass. Residual background was removed in two further steps. The coplanarity of the events (i.e. the condition that in the photon-nucleon center-of-momentum (cm) system, the azimuthal angle between the recoil nucleon momentum and the sum of the meson momenta must be $180^\circ$) was tested. The result is shown in Fig. 2. Background for detection of $\pi^0\eta p$ triples is almost negligible, for $\pi^0\eta n$ triples it is small. In the final step, the missing mass of the events (although the recoil nucleon was detected, it was treated as a ‘missing’ particle) was analyzed as described in [6] for double $\pi^0$ production. The resulting spectra (Fig. 2) were almost background free and the selection criteria indicated in the figure were applied.

The identification of the coherent $\gamma d \rightarrow d\pi^0\eta$ reaction used the same analysis steps for the two neutral mesons. The recoil deuterons were identified in TAPS by a ToF-versus-E analysis. The final step was a missing-mass analysis (the deuteron was treated as missing particle). Typical spectra are shown in Fig. 3. The ToF-versus-E spectrum shows a clear deuteron band structure. The missing-mass spectrum is almost background free and perfectly reproduced by the Monte Carlo simulation (the signal width is much more narrow than for the quasi-free reactions). Also deuterons which were stopped in the TAPS-Veto were accepted. In this case, the ToF-versus-E analysis was based on the signals from the TAPS-Veto detectors (not shown in the figure).

![Fig. 2](image1.png)

*Fig. 2. Left hand side: Coplanarity spectra (see text) for the four different isospin channels (final state nucleons in brackets are spectators, without brackets are detected participants). Black curves: MC simulations of signal reactions. Red and magenta curves (only for Fig. 2): simulated background from $\pi^0\eta^0 p(n)$ final state, bottom, left corner): simulated background from $\pi^0\eta^0 p(n)$ final state. Vertical lines indicate applied cuts. Right hand side: Missing mass spectra for same reactions.*

Fig. 3. Identification of $\gamma d \rightarrow d\pi^0\eta$. Left hand side: missing mass spectrum, vertical lines indicate event selection (only events with missing mass in this range are included in the ToF-versus-E spectrum), (red) curve: Monte Carlo simulation of line shape. Right hand side: ToF-versus-E in TAPS, (red) lines indicate event selection (only events with charged particle in this region included in missing mass spectrum).

The analysis of the $\pi^+\eta$ final state was carried out analogously to the analysis of $\pi^0\pi^\pm$ pairs in [28]. Charged pions...
were selected by the $E - \Delta E$ cut shown in Fig. 1 and the $\eta$ invariant mass peaks were fitted with background polynomials and simulated peak line shapes. This was followed by coplanarity and missing-mass analysis cuts. The results are shown at the bottom of Fig. 2. The only significant background observed was in the coplanarity spectra of the $\pi^+\eta\mu$ final state. It is related to events from the $\gamma d \rightarrow \pi^0\pi^0(p\bar{p})$ reaction, for which one $\pi^0$-decay photon has escaped detection, the other photon from the same $\pi^0$ was misassigned as a neutron, and the proton was misidentified as a charged pion. The shape of this background could be reproduced by Monte Carlo simulations with GEANT4. The background below the 180° peak was subtracted and this was done individually for each data point in the subsequent missing mass spectra. The resolution in the missing-mass spectra is worse than for neutral pions because of the less precise measurement of the energies of the charged pion in the calorimeter. However, there is basically no background visible in the missing mass spectra and the line shapes are well reproduced by Monte Carlo simulations.

Although Figs. 1, 2 show spectra obtained by integration over all incident photon energies and other variables (angles, invariant masses) the actual analysis was performed individually for each bin of photon energy and other variables for differential spectra.

The extracted yields were converted to cross sections using the target surface densities ($0.231 \pm 0.005$ barn$^{-1}$ for most of the beam times, see [28] for details), the incident photon flux, the simulated detection efficiency, and the decay branching ratios [23] of $\pi^0$ ($98.823 \pm 0.034\%$) and $\eta$ ($39.41 \pm 0.20\%$) mesons into photon pairs. More details are given in [29]. The detection efficiency was simulated similarly as in [28,29] with the GEANT4 code [42]. Since the reaction is dominated by the $\Delta^5/2^+ \rightarrow \eta \Delta(1232)$ $\rightarrow \pi\eta N$ chain, the sequential decay with the intermediate $\eta \Delta(1232)$ state was used for the event generator. This generator describes the missing mass distributions (see Fig. 2 and the $\pi\eta$, $\pi N$, and $\eta N$ invariant mass distributions (not shown) very well. The angular distributions deviate not much from isotropy, which was used for the MC (see [14] for angular distributions of the free $\gamma p \rightarrow p\pi^0\eta$ reactions, the results for the other isospin channels are similar). Therefore, the simulation reflects all relevant properties of the reaction. As in [29], corrections for the recoil nucleon detection efficiencies obtained from direct measurements have been applied.

Total cross sections for final states with detected recoil nucleons were analyzed in two ways (see [29] for details). The reconstruction as a function of the incident photon energy profits from the good energy resolution of the spectrometer, but the results are folded in with nuclear Fermi motion. In the second analysis, the Fermi-momentum corrected cm energy $W$ was reconstructed from the kinematics of the final state. This eliminates the Fermi smearing, but introduces effects from experimental resolution (energies and angles measured with the calorimeters) into the $W$ measurement. However, for the present measurement no rapid variations of the cross sections are involved. Both effects are therefore not important. The quasi-free cross section data extracted by the two methods are in good agreement (apart from the immediate threshold region where Fermi motion smears out the excitation function across the free production threshold). Furthermore, an analysis of free proton data with the $W$ reconstruction method (see Fig. 4c) gives an identical result as the use of the incident photon energy (in the latter case neither Fermi motion nor reconstruction resolution enter).

Systematic uncertainties of the data have been discussed in detail in [28,29]. The total overall normalization uncertainty (photon flux, target density) is between 5% (quadratic addition) and 7% (linear addition). Uncertainties from analysis cuts and simulation of the detection efficiency excluding the recoil nucleons are in the range of 5 - 10%. The uncertainty from the recoil nucleon detection efficiency has been estimated in [29] at the 10% level. It can be additionally checked by the comparison of the inclusive cross sections with the sum of the exclusive ones (see Sec. 3). The overall normalization uncertainties cancel in all ratios. The effects from the meson detection cancel almost completely for the $\sigma(\pi^0\eta)/\sigma(\pi^0\eta)$ and for the $\sigma(\pi^+\eta)/\sigma(\pi^-\eta)$ ratios, and partly for the others.

3. Results

The results for the total cross sections are summarized in Fig. 4. Figs. 4a, 4b correspond to the analysis as a function of incident photon energies, Figs. 4c and 4d show the cross sections extracted as a function of reconstructed final state invariant masses. For both types of $\pi\eta$ pairs inclusive cross sections and the summed up exclusive cross sections agree with each other within approximately 5% (this test is only possible for the analysis using incident photon energies since the final state reconstruction requires detection of the recoil nucleons). Deviations for the charged pions are statistically distributed but the deviations for the neutral pions seem to be systematic. A possible systematic effect could arise in the inclusive $\pi^0\eta$ cross section because the event generator used for this reaction did not take into account that events from the coherent reaction have different angular distributions.

Free-proton data from the measurement with the liquid hydrogen target have also been analyzed. In the case of $\pi^0\eta$ pairs, the results are in excellent agreement with previous measurements [14] (see Fig. 4c); the $\gamma p \rightarrow n\pi^+\eta$ reaction has been measured for the first time. The results for the $p\pi^0\eta$ final state are in good agreement with the isobar model of Fix et al. [17] (which is expected because the model was fitted to the existing $p\pi^0\eta$ data), but for the $n\pi^+\eta$ final state agreement is not so good above $W = 1.8$ GeV. In contrast to single $\eta$ production [29], but similar to single $\pi^0$ production [30], there is a significant cross section difference between free and quasi-free results, indicating that final state interaction (FSI) effects are present. FSI seems to be larger for neutral pions than for charged pions (the
same is true for single pion production [27]). Nevertheless, under the assumption that FSI effects are similar for protons and neutrons, cross section ratios can be extracted. They are shown in Fig. 5a. They are in quite good agreement with Eq. 1 and also with the model results from [17]. The ratios for reactions with charged and neutral pions are influenced by the different FSI effects. They are in fact somewhat larger than predicted. The results for the coherent reaction $\gamma d \rightarrow \pi^0 \eta$ are compared in Fig. 5b to model predictions from Egorov and Fix [22] and good agreement is found here. In summary, the isospin dependence of the total cross sections is in excellent agreement with the expectations for a dominant $\Delta 3/2^- \rightarrow \eta\Delta(1232) \rightarrow \pi\eta N$ contribution.

Differential spectra for invariant mass distributions of the $\pi\eta$ pairs and the meson - nucleon pairs have been constructed from full kinematic reconstruction of the final states so that they are not affected by Fermi motion. The invariant mass distributions for reactions of protons and neutrons and for neutral and charged pions are basically identical (after re-normalization of their absolute scales) and in excellent agreement with model predictions from [17].

Fig. 4. Upper row (a): Total cross sections for the $\pi^0\eta N$ final states as a function of incident photon energies. (Blue) squares: $\pi^0\eta$ final state, (red) dots: $n\pi^0\eta$ final state, (black) dots: inclusive $X\pi^0\eta$ analysis, (green) stars: sum of exclusive cross sections. (Light blue) triangles: $\pi^0\eta$ final state from free protons (hydrogen target). Insert: ratio of $\sigma(n,\pi^0)$ to $\sigma(p,\pi^0)$. (b): Corresponding results for the $\pi^\pm\eta N$ final states. (Blue) squares: $\pi^+\eta$ final state, (red) dots: $p\pi^+\eta$ final state, (black) dots: inclusive $X\pi^+\eta$ analysis, (green) stars: sum of exclusive cross sections. (Light blue) triangles: $\pi^+\eta$ final state from free protons. Insert: ratio of $\sigma(p,\pi^+)\sigma(n,\pi^+)$. For (a) and (b) the green bar histograms indicate the difference between inclusive and summed exclusive cross sections. Bottom row (c): Total cross sections for the $\pi^0\eta N$ final states as a function of reconstructed final state invariant mass $W(N_p,\pi^0,\eta)$. Notation for results from this work are the same as for (a); (black) stars: free proton data from Ref. [14]. Model curves from [17]: solid (blue) free proton, dashed (red) free neutron target, (d): Corresponding results for the $\pi^+\eta N$ final states. Notation for data are the same as in (b), for model curves [17] as in (c).
The most prominent feature of this distributions is a pronounced structure in the nucleon - pion invariant mass distributions at the invariant mass of the $\Delta(1232)$ resonance in agreement with the assumption of an intermediate $\eta\Delta$ state in the $\Delta 3/2^-\rightarrow \eta\Delta(1232)\rightarrow \eta\pi N$ reaction chain.

Angular distributions have been analyzed as in [14] in two different cm frames, the canonical and the helicity system. Also the angular distributions do not show much difference between proton and neutron targets or between neutral and charged pions. Agreement with the model predictions from [17] is reasonable for all observables, which is further evidence that the dominating production mechanisms are well understood.

The results for this differential cross sections and also for polarization observables like the beam-helicity asymmetry measured with a circularly polarized photon beam and an unpolarized target will be discussed in a detailed paper following the present letter.

4. Summary and Conclusions

Precise results have been obtained for the photoproduction of $\pi^0\eta$ pairs from free protons, quasi-free protons, quasi-free neutrons bound in deuterium, and coherently from deuterons. Production of $\pi^+\eta$ pairs has been studied for free and quasi-free protons and production of $\pi^-\eta$ pairs for quasi-free neutrons. This means that all possible isospin channels for photoproduction of $\pi\eta$-pairs from nucleons and from the deuteron have now been measured (previous experiments covered only the free $\gamma p\rightarrow p\pi^0\eta$ reaction). The main results can be summarized as follows:

The comparison of free and quasi-free measurements for proton targets indicates significant FSI effects. These effects are quantitatively not precisely understood, but seem to be more important for the comparison of reactions with neutral and charged pions than for the comparison of final states with the same type of pions but different nucleons. This is similar to the photoproduction of single pions which shows also much larger effects for neutral pions due to the different FSI effects in the $np$ system (which can be bound in the final state) compared to the $nn$ and $pp$ systems [27].

The most important results are the cross section ratios for the different isospin channels of the quasi-free production reactions. They allow model independent conclusions about the dominant reaction mechanism. Equation (1) is valid for (I) $\gamma N\rightarrow \Delta^*\rightarrow \Delta\eta\rightarrow N\pi\eta$ and (II) $\gamma N\rightarrow \Delta^*\rightarrow N^*\pi\rightarrow N\pi\eta$ reaction chains, but not for $\gamma N\rightarrow N^*\rightarrow N^*\eta\rightarrow N\pi\eta$ or $\gamma N\rightarrow N^*\rightarrow N^*\pi\rightarrow N\pi\eta$ sequences (for the latter $\sigma(\pi^\pm\eta N)/\sigma(\pi^0\eta N)=2$ would hold and the cross section ratios for neutron and proton targets would depend on the corresponding ratios of the helicity couplings of the primary $N^*$ resonance). This is clear evidence for a dominant contribution from primary excitation of $\Delta^*$ resonances.

After re-normalization of the absolute magnitudes, invariant mass distributions of the $\pi^0\eta$ pairs and the meson - nucleon pairs are in agreement for all four reaction channels. They show the same features already observed for the free $\gamma p\rightarrow p\pi^0\eta$ reaction [9,10,14]. This is in particular a dominant signal from the decay of the $\Delta(1232)$ intermediate state in the $N\pi$ invariant mass. Contributions from the $a_0$ meson in the $\pi\eta$ invariant mass become important only at higher incident photon energies [9,10,14], and the signal from the $N(1535)1/2^-$ intermediate state in the $N\eta$ invariant mass is small.

The experimental results for total cross sections and invariant mass distributions are in good agreement with model predictions from Fix et al. [17] apart from the scale difference for quasi-free reactions due to FSI effects. Also,
the angular distributions are in reasonable agreement with expectations. The good agreement between the total cross section for the coherent $\gamma d \rightarrow d^2\pi^0\eta$ process and the model predictions from Egorov and Fix [22] is further evidence that the isospin decomposition of this reaction is well understood. Altogether, all results support the dominance of the $\Delta_3^-(1700) \rightarrow \eta\Delta(1232) \rightarrow \pi^0\eta p$ reaction chain in the threshold region.

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