Magnet-Free Time-Resolved Magnetic Circular Dichroism with Pulsed Vector Beams

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Abstract

Magnetic circular dichroism (MCD) is a widely used spectroscopic technique which reveals valuable information about molecular geometry and electronic structure. However, the weak signal and the necessary strong magnets impose major limitations on its application. We propose a novel protocol to overcome these limitations by using pulsed vector beams (VBs), which consist of nanosecond gigahertz pump and femtosecond UV-Vis probe pulses. By virtue of the strong longitudinal electromagnetic fields, the MCD signal detected by using the pulsed VBs is greatly enhanced compared to conventional MCD performed with plane waves. Furthermore, varying the pump-probe time delay allows to monitor the ultrafast variation of molecular properties.

Graphical TOC Entry
Over the past decades, magnetic molecules, ranging from simple radicals to single molecule magnets, have opened up potential applications in many areas, such as molecular spintronics, magnetic refrigeration, and electrocatalysis. Various optical spectroscopic techniques have been developed to investigate the electronic and magnetic properties of molecules and understand the magneto-structural correlation, and magnetic circular dichroism (MCD) is one of the most widely used tools. In this technique, a strong static magnetic field is applied to induce Zeeman splitting in molecules by lifting the degeneracy of the electronic states. The MCD signal is then given by the differential absorption of the left- and right-circularly polarized (LCP and RCP) light passing through the molecular sample. MCD has demonstrated its superiority over linear absorption spectroscopy in determining electronic transitions, as well as in revealing information about the degeneracy and symmetry of electronic states.

Despite its rapid progress and wide applications, MCD still faces several challenges: First, being the differential absorption of the LCP and RCP plane waves (PWs), the intensity of conventional MCD signal is generally 2 to 3 orders of magnitude weaker than the absorption signal. Second, a strong static magnetic field is needed to induce the Zeeman splitting in conventional MCD experiments. Although numerous types of magnets have been designed, their practical use can be cumbersome, because of the required large-sized devices and cryogenic temperatures.

The first challenge concerning weak signal can be overcome by replacing the LCP and RCP PWs by left- and right-circularly polarized beams with nonzero longitudinal components (LCPL and RCPL), which are realized by superposing the azimuthally and radially polarized (AP and RP) vector beams (VBs). It has been proposed that VBs could greatly enhance the circular dichroism (CD) signals of chiral molecules, thanks to the strong electromagnetic fields generated by the VBs. However, it is difficult to probe time-varying molecular properties with continuous-wave VBs, which raises a third challenge for MCD measurements.
Inspired by the recent progress in the design and implementation of V Bs\textsuperscript{[19,26\textendash}28] and gigahertz (GHz) spectroscopy,\textsuperscript{[29,30]} in this work we propose a novel protocol for magnet-free time-resolved MCD measurements, which utilizes pulsed V Bs and will be denoted V BMCD.

V Bs have cylindrical symmetry along the beam axis. In the cylindrical coordinate system, the electric and magnetic fields of a pulsed AP VB are expressed as

\[
\mathbf{E}_A(r, t) = \hat{\phi} \mathbf{H}(r) e^{i(Kz - \Omega t)} G(t), \quad (1)
\]

\[
\mathbf{B}_A(r, t) = \hat{\rho} \left( -\frac{K}{\Omega} \right) + \hat{z} \left( -\frac{i}{\Omega} + \frac{1}{\rho} \frac{\partial}{\partial \rho} \right) \mathbf{H}(r) e^{i(Kz - \Omega t)} G(t). \quad (2)
\]

Here, \(\hat{\rho}, \hat{\phi},\) and \(\hat{z}\) represent the radial, azimuthal, and longitudinal unit vectors, respectively; \(r \equiv (\rho, \phi, z)\), and \(\Omega\) is the central frequency. The spatial profile assumes a Hermite-Gaussian form,\textsuperscript{[26]}

\[
\mathbf{H}(r) = A_0 \frac{4\rho}{\sqrt{\pi|W(z)|^2}} \exp \left[ -\frac{\rho^2}{|W(z)|^2} \right] \exp \left[ \frac{iK\rho^2}{2R(z)} \right] \exp \left[ -2i \arctan \left( \frac{z}{z_R} \right) \right], \quad (3)
\]

where \(A_0\) is the amplitude, \(K\) is the wavenumber, \(W_0\) is the beam waist, \(z_R = \frac{1}{2}KW_0^2\) is the Rayleigh length, \(W(z) = W_0\sqrt{1 + z^2/z_R^2}\) is the beam width, and \(R(z) = z + z_R^2/z\) is the radius of curvature. The temporal profile assumes a Gaussian form,

\[
G(t) = \exp \left[ -4\ln2 \frac{(t - T_c)^2}{\tau_D^2} \right], \quad (4)
\]

with \(T_c\) and \(\tau_D\) being the central time and the duration time, respectively. The corresponding electric and magnetic fields of the pulsed RP VB are respectively\textsuperscript{[26]}

\[
\mathbf{E}_R(r, t) = \hat{\rho} + \hat{z} \left( \frac{i}{K} \right) \left( \frac{1}{\rho} + \frac{\partial}{\partial \rho} \right) \mathbf{H}(r) e^{i(Kz - \Omega t)} G(t), \quad (5)
\]

\[
\mathbf{B}_R(r, t) = \hat{\phi} \left( \frac{K}{\Omega} \right) \mathbf{H}(r) e^{i(Kz - \Omega t)} G(t). \quad (6)
\]

In this work the 0.1 \(\sim\) 10 T static magnetic field typically used in conventional MCD is
Figure 1: (a) Schematic of the proposed VBMCD protocol. The red cylinder represents the paraxial region where a strong localized magnetic field generated by the pump VB exists. \( \hat{\rho} \) and \( \hat{z} \) denote the radial and longitudinal directions, and \( T_c \) and \( t_c \) are the centers of pump and probe pulses, respectively. (b) Variation of \( |B_z| \) with respect to \( \rho \), where \( W_0 \) is the pump beam waist. (c) Vector field plots of the LCPL and RCPL probe VBs.

replaced by a temporally- and spatially-varying magnetic field \( B(r, t) = B_A(r, t) \), which is generated by an AP VB (Figure 1b). The longitudinal component of \( B_A \), denoted as \( B_z \), is tightly localized around the beam axis, and its amplitude decreases rapidly with the radial distance \( \rho \) (Figure 1b). To create an appreciable Zeeman splitting in the molecule, a pulsed VB is utilized as the pump beam to supply a strong longitudinal field \( B_z \). Two pulsed probe beams, LCPL and RCPL (Figure 1c), which are collinear with the pump VB, are employed to measure the MCD signals. The electric and magnetic fields of the probe pulses
are explicitly expressed as

\[
\begin{pmatrix}
E_j(r,t) \\
B_j(r,t)
\end{pmatrix} = -\frac{1}{\sqrt{2}} \begin{pmatrix}
E_A(r,t) & E_R(r,t) \\
B_A(r,t) & B_R(r,t)
\end{pmatrix} \begin{pmatrix}
c_j \\
i
\end{pmatrix},
\]

where \( c_j = 1 \) for \( j = \text{LCPL} \) and \( -1 \) for \( j = \text{RCPL} \), and \( E_A/R \) and \( B_A/R \) denote the electric and magnetic fields of the AP/RP VBs for designing the LCPL and RCPL, respectively. The spatial and temporal profiles of the probe VBs, denoted as \( H(r) \) and \( G(t) \), have the same forms as those of the pump, but the values of the involving parameters are different. These include amplitude \( A_0 \), wavenumber \( k_j \), beam waist \( w_0 \), pulse central time \( t_c \) and duration time \( \tau_d \).

To ensure that the Zeeman states are detectable by the probe VBs, the strength of localized magnetic field should reach \( 0.1 \sim 10 \text{ T} \). Moreover, to acquire nonzero time-averaged MCD signal with the oscillatory pump pulse, the duration of the probe pulses should be much shorter than that of the pump pulse, so that the longitudinal magnetic field \( B_z \) of the pump beam is almost unchanged during the action of the probe pulse. These suggest the use of a nanosecond GHz pump pulse and femtosecond UV-Vis probe pulses. Generation of such pulsed VBs is well within the capabilities of current technology. Furthermore, the time delay between the pump and probe pulses can be precisely tuned, thus allowing for the detection of time-varying molecular properties.

In the following, we compare the VBMCD signal to conventional MCD. The light-matter interaction Hamiltonian for our setup is \( H_{\text{int}} = -\hat{\mu} \cdot E_j - \hat{m} \cdot B - \frac{1}{2} \hat{Q} : \nabla E_j + \text{H.c.} \), where \( \hat{\mu} \), \( \hat{m} \), and \( \hat{Q} \) are the electric transition dipole, magnetic transition dipole, and electric transition quadrupole operators, respectively. The contribution of the electric quadrupole term to the MCD signal vanishes when performing rotational averaging over randomly oriented molecules in solutions or in the gas phase. The interactions between the molecular transition dipoles and the electric component of the pump VB and the magnetic component of the probe pulses are neglected, because the former is off-resonant with the electronic excitations in molecules.
due to much lower frequency of the pump pulse, while the latter is several orders of magnitude weaker than $-\mu \cdot E_j$.

The wavenumber $k_j$ of the LCPL and RCPL pulses can be obtained by first-order time-dependent perturbation theory,\cite{ref} see Section S1 in the Supporting Information (SI). Their difference, $\Delta k \equiv k_{\text{LCPL}} - k_{\text{RCPL}}$, which largely determines the lineshape of the MCD spectrum, is expressed as the sum of three Faraday terms, denoted by $A(\omega), B(\omega)$ and $C(\omega)$, as follows,

$$
\Delta k(\omega) = \frac{n\mu_0 c}{3\hbar^2} B_z(r, t) [A(\omega) + B(\omega) + C(\omega)], \quad (8)
$$

$$
\Lambda(\omega) = \tilde{\Lambda}(\omega, \Omega) + B_z(r, t) \frac{\partial f_{l, g}}{\partial \omega} \tilde{\Lambda}(\omega, -\Omega), \quad \Lambda \in \{A, B, C\}, \quad (9)
$$

$$
\tilde{A}(\omega, \Omega) = i (\omega + \Omega)^2 \sum_{g, l_\beta} \sum_{g', l_\beta'} \frac{\partial f_{l, g}}{\partial \omega} \left[ f_{l, g}(\omega) + f_{l, g}(\omega + \Omega) \right] \left\{ \sum_{v, v' \neq g} \left( \frac{\mu_{l_\beta g, l_\beta'} \cdot m_{g, g, l_\beta}}{\Omega + \omega_{l_\beta g}} + \frac{\mu_{l_\beta g, g, l_\beta'} \cdot m_{l_\beta g, g}}{\Omega + \omega_{l_\beta g}} \right) \right\}, \quad (10)
$$

$$
\tilde{B}(\omega, \Omega) = -i (\omega + \Omega)^2 \sum_{g, l_\beta} \sum_{g', l_\beta'} \frac{\partial f_{l, g}}{\partial \omega} \left[ f_{l, g}(\omega) + f_{l, g}(\omega + \Omega) \right] \left\{ \sum_{v, v' \neq g} \left( \frac{\mu_{l_\beta g, l_\beta'} \cdot m_{g, v}}{\Omega + \omega_{l_\beta g}} + \frac{\mu_{l_\beta g, v'} \cdot m_{g, l_\beta}}{\Omega + \omega_{l_\beta g}} \right) \right\}, \quad (11)
$$

$$
\tilde{C}(\omega, \Omega) = -i (\omega + \Omega)^2 \frac{\hbar}{2N_g} \sum_{g, l_\beta} f_{l, g}(\omega + \Omega) \left( \frac{\mu_{l_\beta g, l_\beta'} \cdot m_{g, g}}{\Omega + \omega_{l_\beta g}} \right). \quad (12)
$$

Here, $n$ is the molecular concentration, $\mu_0$ is the magnetic permeability, $c$ is the speed of light, and $f_{l, g}(\omega) \equiv (\omega - \omega_{l \beta g} + i\eta)^{-1}$, with $g$ and $l_\beta$ labeling the states in the degenerate sublevels of the ground ($g$) and excited ($l$) states, respectively. $T$ is the temperature, $N_g$ is the degeneracy of the ground state manifold, $\mu_{l \beta g}$ and $m_{l \beta g}$ denote the electric and magnetic transition dipole moments between states $l_\beta$ and $g$, respectively. The expressions in Equations (10)--(12) reduce to their counterparts for the conventional MCD when the pump central frequency $\Omega = 0$. Therefore, the conventional MCD spectrum measured with PW beams can be recovered by replacing $B_z$ with a static magnetic field $B_z$ (Section S1 in
The Faraday $A$, $B$ and $C$ terms in Equation (8) are functions of the probe central frequency $\omega$. They provide valuable information about the degeneracy and symmetry of electronic states. Specifically, the $A$ term arises from the Zeeman splitting of orbitally degenerate excited states. It has a characteristic derivative lineshape and is independent of temperature. The $B$ term originates from the magnetic-field-induced mixing of the zero-field nondegenerate states. It is also temperature-independent, but usually much smaller compared to the other two terms. The $C$ term exhibits a strong inverse-temperature dependence. It reveals the information about the ground state population in the presence of the Zeeman splitting due to the external magnetic field, and is nonvanishing only for molecules with degenerate ground states.

For a PW beam, the longitudinal components of electric and magnetic fields are absent, and thus the luminous flux (magnitude of Poynting vector) is entirely along the axial direction of beam. Consequently, the flux can be gathered only in the longitudinal direction for the conventional MCD. In contrast, VBs have strong longitudinal components of electric and magnetic fields, and the luminous flux is nonzero in the radial direction. By using a cylindrical sample cuvette aligned coaxially with the probe pulses (Figure 1a), the luminous flux in the radial direction, gathered by the detector placed at a given azimuthal angle $\phi$, is

\[
I_{\rho}(\omega, \tau_c; k_j) = \frac{1}{\mu_0} \int dt \int_0^P \rho \mathbf{E}_j \times \mathbf{B}_j^* \cdot d\mathbf{\rho} + \text{c.c.},
\]

with $P$ being the radius of interaction cross section between the probe beams and the molecular sample. Because of their cylindrical symmetry, both $\mathbf{E}_j$ and $\mathbf{B}_j$ are independent of $\phi$, and hence the luminous flux $I_{\rho}(\omega, \tau_c; k_j)$ detected at any $\phi$ is identical. Therefore, using a ring-like detector encircling the axis of cuvette is most favourable for the collection of luminous flux.

The linear absorption spectrum is

\[
\epsilon_{\rho}(\omega, \tau_c; k_j) = (n_0 L)^{-1} \ln[I_{\rho}(\omega, \tau_c; k_j)/I_{\rho}(\omega, \tau_c; k_0)],
\]

where $\tau_c$ is the time delay between the pump and probe pulses, $n_0$ is a reference molecular concentration, $L$ is the length of the sample cuvette, and $k_0 = \omega/c$ is the wavenumber of the probe.
VBs in vacuum. The resulting VBMCD spectrum is explicitly expressed as

\[
\Delta \epsilon_\rho(\omega, \tau_c) \equiv \epsilon_\rho(\omega, \tau_c; k_{LCPL}) - \epsilon_\rho(\omega, \tau_c; k_{RCPL}) = \frac{1}{n_0 L} \ln \left[ \frac{I_\rho(\omega, \tau_c; k_{RCPL})}{I_\rho(\omega, \tau_c; k_{LCPL})} \right].
\]  

(13)

Clearly, the VBMCD spectroscopic signal characterizes the difference between the linear absorption spectra measured by the LCPL and RCPL beams, rather than their absolute amplitudes. Thus, the intensity of the VBMCD signal should be distinguished from that of luminous flux collected by the detector. Particularly, although the luminous flux in the radial direction is relatively weaker than in the longitudinal direction, it is sufficiently bright to be harvested by modern detectors. Therefore, the VBMCD signal can be significantly enhanced over that of the conventional MCD, even with a relatively weaker luminous flux received by the detector.

To elucidate the origin of signal enhancement, we express the VBMCD spectrum \( \Delta \epsilon_\rho \) as

\[
\Delta \epsilon_\rho(\omega, \tau_c) \approx \frac{\text{Im}[\Delta \tilde{k}(\omega)]}{n_0} \frac{X(\tau_c)Y(\zeta_P)Z(\zeta_P)}{2\zeta_L^2}.
\]  

(14)

Here, \( \zeta_L \equiv L/w_0 \) and \( \zeta_P \equiv P/w_0 \) are the reduced path length and reduced radius of the cuvette, respectively, with \( w_0 \) being the probe beam waist. \( \Delta \tilde{k}(\omega) \) is \( \Delta k(\omega) \) evaluated at \( \tau_c = 0 \) and \( \rho = W_0 \). It dominates the lineshape of the VBMCD spectrum, which resembles closely the conventional MCD spectrum. \( X(\tau_c) \), \( Y(\zeta_P) \) and \( Z(\zeta_P) \) are three characteristic functions which determine the intensity of the measured spectrum (see Section S1 in the SI for more details). They are independent of the molecular details. Specifically, \( X(\tau_c) \) is a time-varying function whose temporal profile is almost identical to that of the pump pulse (see Figures 1a and 2a). \( Y(\zeta_P) \) and \( Z(\zeta_P) \) are enhancement factors which originate from the strong longitudinal electromagnetic fields generated by the pump and the probe VBs, respectively. Particularly, the \( Z \) factor increases drastically with the decrease of \( \zeta_P \) (Figure 2b). Moreover, the intensity of the VBMCD signal is inversely proportional to the
quadratic of $\zeta_L$. Therefore, using a shorter and thinner sample cuvette is generally more favorable to achieve an enhanced VBMCD spectrum. Nevertheless, in practice the sample cuvette cannot be too small, because too few molecules could make the luminous flux in the radial direction too weak to detect or the signal-to-noise ratio too low.

To demonstrate the utility of the proposed VBMCD protocol, we perform simulations for the MCD signals of the hydroxyl (OH) radical (Section S2 in the SI). Figures 2c and 2d depict the lineshape and intensity of the VBMCD spectrum, which are compared in parallel with the conventional MCD spectrum $[\Delta \varepsilon_{PW}(\omega)]$ probed by PWs (see Equation S12 in the SI for more details). The Faraday $A, B$ and $C$ terms of the VBMCD spectrum agree closely
with their counterparts of the conventional MCD spectrum. This confirms that the VBMCD protocol reproduces all the important spectroscopic information rendered by conventional MCD.

By definition, it is clear that the signal acquisition time does not affect the magnitude of absorption or MCD spectra, but does affect the signal-to-noise ratio in an experiment. Hence, in order to compare the VBMCD and conventional MCD spectra on an equal basis and to accentuate the importance of the enhancement factors, in our simulations we assume that all measurements are performed with sufficiently high signal-to-noise ratio with long enough acquisition time and that the VBs and PWs are equally affected by the optical elements (not shown in Figure 1). In Figure 2d, the localized magnetic field $B_z$ generated by the pump pulse has a peak value of 0.74 T, about 10 times weaker than the static magnetic field $B_z$ (∼ 7.4 T) adopted for the conventional MCD. However, it is remarkable to see that the intensity of $\Delta \epsilon_\rho(\omega)$ is 500 times stronger than the conventional MCD $\Delta \epsilon_{PW}(\omega)$. Although the intensity of both VBMCD signal and conventional MCD signal scales linearly with the magnetic field (see Equation 8 and Section S1 in the SI), the radially detected VBMCD signal can be considerably enhanced by properly adjusting the enhancement factors in Equation 14, which is not possible for the conventional MCD. These results verify that the enhancement factors associated with the radial detection scheme cause the significant enhancement of the VBMCD signal in Figure 2d. Moreover, a pulsed VB is superior to a continuous-wave VB as the pump, since the former can yield a stronger transient magnetic field by consuming the same amount of power. It is possible to further enhance the VBMCD signal by tailoring the VBs. For instance, by aiming the AP VB to a metallic circular aperture, the amplitude of $B_z$ can be further amplified by ∼ 3.8 times, reaching a peak value of 2.8 T (see Section S1 in the SI for more details). Specifically, by setting the probe beam waist, and the radius and length of the sample cuvette to $w_0 = 1$ mm, $P = 0.1$ mm and $L = 0.03$ mm, respectively, the VBMCD signal will reach an intensity about 4 orders of magnitude stronger than the conventional MCD.
Figure 3: Simulated time-resolved VBMCD spectra of OH radicals, $\Delta \epsilon_\rho(\omega, \tau_c)$, in two scenarios characterized by the time-varying molecular concentration: (a) $n(t) = n_0 e^{-rt}$ and (b) $n(t) = n_0(1 - e^{-rt})$, with the rate constant $r = 1 \text{ ns}^{-1}$. Both scenarios adopt two temporally separated pump pulses centered at $T_c = 1 \text{ ns}$ and $3 \text{ ns}$, and the vertical plane at $t = 2 \text{ ns}$ (indicated by dashed lines) marks the center of interval between the two pump pulses. Note that the time delay has been converted to the probe central time, i.e., $t_c = T_c + \tau_c$. The other parameters adopted for the simulations are listed in Section S3 in the SI.
Pulsed VBs enable a magnet-free experimental protocol and achieve a substantial enhancement of MCD signals, and further allow for the detection of real-time dynamics of molecular systems by tuning the time delay between the pump and probe pulses. In the present time-resolved VBMCD protocol, the pump pulses do not trigger any dynamic change of molecules. Instead, they impose weak perturbation on the molecular electronic states by creating Zeeman splitting, so that the molecules become discernible to the subsequent probe pulses.

As a demonstration, we consider two scenarios, in which OH radicals are consumed or produced at the nanosecond time scale, respectively. The corresponding time-resolved VBMCD spectra, $\Delta \epsilon_\rho(\omega, \tau_c)$, are displayed in Figure 3a and 3b. In each scenario, two temporally separated pump pulses are applied, and the relative intensities of the MCD signal detected at the probe central time $t_c$ directly reflect the change in molecular concentration over time, since $\Delta \epsilon_\rho \propto n(t)$. The signal changes its sign periodically with $t_c$, due to the $X(\tau_c)$ factor in Equation 14 and the signal intensity reaches its maximum when the pump-probe time delay is zero, because the corresponding pump magnetic field is the strongest. In Figure 3a, the signal intensity is much reduced at the second pump pulse, which reveals a rapid drop in concentration; whereas in Figure 3b, the signal is somewhat enhanced at the second pump pulse, indicating a mild increase in concentration.

As inferred from Equations 8 and 14, the time dependence of the VBMCD spectra is governed by the molecular concentration $n(t)$ and the pump magnetic field $B_z(r, t)$, and the parameters for the latter are already known and can be precisely controlled when conducting an experiment. Therefore, by performing the calculation for $\Delta \epsilon_\rho(\omega, \tau_c)/B_z(r, t)$, we can extract the time-dependent molecular concentration from the measured VBMCD spectra. As exemplified in Figure 4, the calculated data for the OH radical consumption and production processes (Figure 3) agree closely with the actual concentrations. Hence, the time-resolved VBMCD signal provides a route to extract information about the real-time variation of the molecular concentration.
Figure 4: Real-time variations of OH radical concentration calculated by $\Delta \epsilon_p(\omega, \tau_c)/B_z(r, t)$ for the two scenarios explored in Figure 3. The actual variations of $n(t)$ are also plotted for comparison. The frequency $\omega$ is fixed at $\omega = 34250$ cm$^{-1}$. The other parameters adopted for the simulations are listed in Section S3 in the SI.

Note that, in addition to the dynamic variation of molecular concentration at the nanosecond time scale, the proposed protocol may be conveniently generalized to the investigation of geometric and electronic dynamics of magnetic molecules or materials at the picosecond time scale, e.g., the ultrafast magnetization of ferromagnets triggered by a certain driving source. This can be achieved by adopting a picosecond pump AP VB in our protocol. Therefore, the time-resolved VBMCD protocol offers a useful spectroscopic tool for monitoring ultrafast dynamic process of molecules.

To conclude, we have theoretically designed an efficient protocol for realizing the significantly enhanced magnet-free MCD measurement, where the strong longitudinal magnetic field of the nanosecond GHz AP VB induces the Zeeman splitting in the molecules, and the femtosecond UV-Vis LCPL/RCPL enables the enhancement of the MCD signal. Furthermore, the time-resolved signal obtained by varying the pump-probe time delay promises to
unravel transient molecular dynamics on the nanosecond time scale. The proposed protocol is currently feasible and may boost the investigation of ultrafast dynamic processes in magnetic molecules and materials.

**Supporting Information Available**

All other data supporting this work, including derivation of the formulas of the VBMCD spectrum, quantum chemistry calculations for the VBMCD spectrum of the OH radicals, and parameters adopted for the simulations illustrated in Figures 2, 3 and 4 are provided in the Supporting Information.

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