Detection of multiple waves for COVID-19 and its optimal control through media awareness and vaccination: study based on some Indian states

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Abstract COVID-19 is a highly infectious disease, and in very recent times, it has shown a massive impact throughout the globe. Several countries faced the COVID-19 infection waves multiple times. These later waves are more aggressive than the first wave and drastically impact social and economic factors. We developed a mechanistic model with imperfect lockdown effect, reinfection, transmission variability between symptomatic & asymptomatic, and media awareness to focus on the early detection of multiple waves and their control measures. Using daily COVID-19 cases data from six states of India, we estimated several important model parameters. Moreover, we estimated the home quarantine, community, and basic reproduction numbers. We developed an algorithm to carry out global sensitivity analysis (Sobol) of the parameters that influence the number of COVID-19 waves ($W_C$) and the average number of COVID-19 cases in a wave ($A_W$). We have identified some critical controlling parameters that mainly influenced $W_C$ and $A_W$. Our study also revealed the best COVID-19 control strategy/strategies among vaccination, media awareness, and their combination using an optimal cost-effective study. The detailed analysis suggests that the severity of asymptomatic transmission is around 10% to 29% of that of symptomatic transmission in all six locations. About 1% to 4% of the total population under lockdown may contribute to new COVID-19 infection in all six locations. Optimal cost-effective analysis based on interventions, namely only vaccination (VA), only media awareness (ME), and a combination of vaccination & media (VA+ME), are projected for the period March 14, 2020, to August 31, 2021, for all the six locations. We have found that a large percentage of the population (26% to 45%) must be vaccinated from February 13 to August 31, 2021, to avert an optimal number of COVID-19 cases in these six locations.

Keywords COVID-19 · Mathematical model · Estimation · Multiple waves · Optimization

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1 Introduction

In December 2019, novel coronavirus disease 2019 (COVID-19) caused by severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2) was first observed in Wuhan, China, and spread all over the world in a very short duration [64]. The World Health Organization (WHO) carefully examined various characteristics of COVID-19 and declares this outbreak as a pandemic [65]. As of January 23, 2022, more than 352.2 million confirmed cases and over 5.6 million deaths due to COVID-19 are reported across the globe [22]. Moreover, 39.5 million confirmed cases and 4.8 lakh deaths due to COVID-19 are reported in India in the same period [22]. Mainly five subtypes of coronaviruses have been identified, e.g., Alpha, Beta, Gamma, Delta, and Omicron, and SARS-CoV-2 is a form of Beta coronavirus [18,46,54].

The initial impact of COVID-19 was catastrophic for almost all countries throughout the globe. As a preventive measure, most of the countries implemented a complete or partial lockdown together with several other preventive measures such as wearing a mask, social distancing, etc., to reduce the contact rate. However, after a certain time, i.e., at the end of the first wave, most of the countries lifted strict lockdown and other measures, which probably leads to other waves of infection. These later waves are more aggressive than the first wave and have a drastic impact on social and economic factors [61]. Currently, COVID-19 multiple waves hit several countries like the USA, India, Brazil, Russia, France, etc. Various studies deal with the causes, prevention, and projection of multiple waves as it has a very calamitous impact on a country. Kaxiras et al. [27] studied the impact of different social distancing factors on multiple waves of COVID-19. A multiple wave model was developed and analyzed the data from several countries in multiple wave scenarios. They also studied the peak intensities of the waves and concluded about the effectiveness of various intervention measures. In their paper, Leung et al. [34] studied a SIR model and discussed the possibility of a second wave based on the relaxation of some preventive measures after the first wave of COVID-19 infection. They have suggested that effective reproduction rate and confirmed case-fatality risk are two critical factors to control the second wave. Hassan and Mahmoud [19] considered a modified SEIR model and studied the impact of COVID-19 multiple waves on US healthcare networks, causes from states reopening during the Fall and Winter seasons. They have observed that the hospitalized cases drastically rise in several regions during the second and third waves. They also showed that protective measures play a vital role and soften these may cause other waves of uncontrollable disease spread in some countries. Cheetham et al. [7] predicted the optimal level of social distancing that could prevent further COVID-19 waves. They warned against the complete lifting of the lockdown after the first wave and projected about a more severe second wave based on the intensive levels of social contact.

Awareness of the people through media is a powerful tool to curb the disease propagation during an infectious disease outbreak [29,53]. It has already been established that media awareness changes the population behavior, which leads to modifying the disease spread [43,69]. As COVID-19 is a highly infectious disease, the role of media is a crucial controlling factor during this pandemic period. Media reporting helps the people to gain knowledge about COVID-19 and act accordingly by taking various protecting measures (e.g., wearing masks, keeping social distancing, sanitization, etc.) to save themselves as well as the community [15]. Many studies focused on the impact of media awareness and suggested that it is a very effective non-pharmaceutical intervention in the absence of vaccines. Although there are recently various vaccines available, the continuous flow of media awareness is needed to control the spread of COVID-19 completely. In their paper, Kobey [28] analyzed an SEIR model to study the impact of media awareness programs on the spread of COVID-19 and suggested that the most effective strategies for controlling or eradicating the spread of COVID-19 by isolating a fraction of susceptible from infective. Zhou et al. [69] considered a compartment model with media programs as a separate state variable and suggested that besides improving the medical levels, media coverage may be an effective way to mitigate the disease spreading during the initial stage of an outbreak. Recently, Taki et al. [60] studied a stochastic model to investigate the impact of media awareness on the spread of COVID-19 and studied the disease extinction scenario. They concluded that the media efforts could be helpful to reduce the number of infectives and offer more time to the authorities to react to the global pandemic. In this context, Sooknnanan and Mays [57] performed an interesting study based on the
contribution of social media in the spread of COVID-19 pandemic.

To eradicate COVID-19 completely, the vaccine is an essential component and its impact together with other interventions must be studied. Apart from non-pharmaceutical interventions, several vaccines have recently been developed and used throughout the globe. However, besides a safe and effective vaccine becomes available, there are several logistical and operational challenges associated with its coverage [13,41]. Many researchers have recently studied the impact of the vaccine to mainly explore its efficacy, required percentage of the vaccinated population to control the epidemic, vaccine distribution strategy, etc. In their paper, Mukandavire et al. [41] studied a compartmental model to study the vaccine efficacy in South Africa. They concluded that vaccine efficacy of at least 70% and very high coverage is required to control the spread of COVID-19. An extensive study was performed by [24] based on several vaccination strategies and their effect on COVID-19 mortality. An age structure mathematical model was considered by [40] to explore the impact of vaccines with several non-pharmaceutical interventions (NPIs). They concluded that only vaccination could not contain the COVID-19 outbreak, but it may be combined with NPIs to control the disease. In their work, MacIntyre et. al. [39] explored vaccination strategies for COVID-19 and the population herd immunity in the state of New South Wales, Australia. They projected that a vaccine with 90% efficiency can create a herd immunity if at least 66% population are vaccinated. They also added that people should be vaccinated at a very fast rate (e.g., 60,000 doses per day) to gain quick control over the disease. Herd immunity against COVID-19 may not be possible if a vaccine has an efficacy of less than 70%. However, the optimal vaccination strategy is advantageous in this context, but we also need to consider various associated costs in a practical situation. Several articles have been published on the optimal control strategy applied to vaccine administration [36], transmission risk [42], non-pharmaceutical interventions [44], etc., in the context of COVID-19. Since media awareness and vaccination are both effective measures against COVID-19 and have not been explored much, it will be interesting to study the overall optimized cost with both of these interventions.

In the present paper, we developed a new mathematical model on COVID-19 with imperfect lockdown effect, reinfection, transmission variability between symptomatic & asymptomatic, and media awareness. Using daily COVID-19 cases data from six states, namely Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB), respectively, for the time period March 14, 2020, till May 12, 2021, we estimated several important epidemiological parameters of the new COVID-19 model. To measure the severity of transmission occurring from home-quarantined and community population, we estimated the home-quarantined (symptomatic and asymptomatic) reproduction number, the community (symptomatic and asymptomatic) reproduction number, and the basic reproduction number for the six mentioned locations. We developed an algorithm to carry out a variance based global sensitivity analysis technique based on Sobol’s method to identify key epidemiological model parameter/parameters that influence the number of COVID-19 waves and the average number of COVID-19 cases in a wave in a location. Finally, an optimal cost-effective study is carried out to determine the best COVID-19 control strategy/strategies among vaccination, media awareness, and their combination to reduce the number of COVID-19 cases in the six mentioned locations at a minimum cost.

2 Method

2.1 Model formulation

We developed a mechanistic model on SARS-CoV-2 that focused on studying the mechanism behind multiple COVID-19 waves in six Indian states, namely Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB). We assume the total human population in a location are subdivided into seven mutually exclusive subclasses Susceptible ($S$), Home-quarantined ($S_L$), Exposed ($E$), Asymptomatic ($I_A$), Symptomatic ($I_S$), Notified cases ($H$), and Recovered ($R$). As COVID-19 is a highly contagious disease, therefore, it is expected that Awareness campaigns (e.g. TV, Newspapers, Social media, Govt. camps, etc.) will gradually increase as the disease progress over time [14, 23, 45]. Therefore, we also considered a Media & awareness density compartment ($M$) in addition to the human compartments.
Furthermore, the COVID-19 model developed in this manuscript is an extension of our earlier work [50]. Below we provided the point-wise extension of the previous work [50]:

1. We considered a fraction ($\theta$) of the home-quarantined population ($S_L$) maintain proper social distancing and therefore do not mix with the community. Thus, remaining fraction ($1-\theta$) of $S_L$ can mix within the community, therefore, getting infection in contact with community symptomatic ($I_S$) and asymptomatic ($I_A$).

2. At the beginning of the epidemic, high density of awareness campaign leads to a larger percentage of the home-quarantined population. However, we assume that this percentage approaches a constant value as the disease progresses. Therefore, we have modified the bilinear awareness response function considered in Kumar et al. [30] by considering a saturating awareness response function $\psi_{SM}$, where $\psi$ is the awareness response intensity of the susceptible individuals.

3. Reinfection with COVID-19 can be possible after exposure to a high virus load [1, 12]. Prolonged virus shedding could be found among COVID-19 recovered patients [35, 38], and therefore, they are advised to home isolation after the recovery. Therefore, we assume that a fraction of the recovered population ($R$) moved to the home-quarantined compartment ($S_L$) after the period ($\frac{1}{\omega_t}$) of natural immunity.

4. We assume that a fraction ($\xi$) of the COVID-19 notified cases ($H$) are critical patients, and they required treatment. Natural recovery rate ($\gamma_2$) of the treated person modified by relative rate of recovery $\lambda$. Currently, there is no effective medicine for the COVID-19. Therefore, we assume that the modification parameter $\lambda$ is greater than zero. Furthermore, we also assume that non-critical fraction ($1-\xi$) of the notified cases get natural recovery at a rate $\gamma_2$.

5. Awareness density ($M$) increases in proportion to a number of notified COVID-19 patients ($H$) in the population. With a limited budget to carry out an awareness campaign, we assume a saturated type growth rate of awareness density ($M$). We assume that the awareness campaign degraded at a rate $d$.

Therefore, following [50] and the assumptions (1) to (5), we have the following system of equation that represent the dynamics of COVID-19:

$$\frac{dS}{dt} = \Pi + \alpha S_L - IS - \mu S - \frac{\beta S I_S}{N - \theta S_L - H} - \frac{\rho \beta S I_A}{N - \theta S_L - H}$$

$$\frac{dS_L}{dt} = \psi_{SM} \frac{1}{1+M} + IS - \mu S_L - \omega S_L - \frac{\beta (1-\theta) S_L I_S}{N - \theta S_L - H}$$

$$\frac{dI_S}{dt} = \frac{\rho \beta (1-\theta) S_L I_A}{N - \theta S_L - H} + \omega S L + (\sigma + \mu) E.$$
### Table 1 Parameters with their respective epidemiological information for the mechanistic ODE model (2.1) for COVID-19

| Parameters | Biological meaning | Value/ranges | References |
|------------|--------------------|--------------|------------|
| N          | Total population   | Varies over locations | [58] |
| 1/μ        | Average life expectancy at birth | Varies over locations | [37] |
| π = μ × N  | Recruitment rate of human population | Varies over locations | [37, 58] |
| β          | Average transmission rate of a symptomatic COVID-19 infected | (0–10) day⁻¹** | [32] |
| ρ          | Transmission variability factor between symptomatic and asymptomatic infection | (0–1)** | [5, 59] |
| ψ          | Awareness response intensity | (0–1) day⁻¹*** | [30, 68] |
| θ          | Fraction of home-quarantined population who maintain social distancing | (0–1)** | [8] |
| 1/σ        | Average incubation period of COVID-19 | 5.1 days | [31, 62] |
| χ          | Average fraction of the COVID-19 exposed population that become asymptomatic infected | (0–1)** | [66] |
| 1/γ₁       | Infectious period of asymptomatic cases | 8 days** | [6] |
| 1/γ₂       | Infectious period of symptomatic cases | 18.0505 days** | [6] |
| τ          | Average hospitalization & notification rate for the COVID-19 symptomatic individuals | (0–1) day⁻¹*** | [50] |
| δ          | Average death rate due to COVID-19 infection | Estimated from COVID-19 data* | [21] |
| ξ          | Average fraction of critical COVID-19 cases that received treatment | 0.1 | [9] |
| λ          | Recovery modification factor | ≥ 0** | [49] |
| l          | Average lockdown rate | (0–0.9) day⁻¹** | [50] |
| 1/ω        | Lockdown period in India | 68 days | [56] |
| 1/ωᵣ       | Period of natural immunity in COVID-19 | (1–8) months** | [12] |
| a          | Awareness growth rate | 0.01 day⁻¹ | [30, 68] |
| d          | Awareness degradation rate | 0.06 day⁻¹** | [30, 68] |
| p          | Rate of vaccination | (0–1) day⁻¹ | [49] |
| ζ          | Covishield Vaccine efficacy | 0.704 | [4] |

**Estimated parameters, *Average COVID-19 death rate (δ) = \( \frac{D}{t \times C} \), \( D \), \( C \), and \( N_t \) are total deaths, total cases and total number of data points, respectively**

**Fig. 1** Flow diagram of the model (2.1)
Fig. 2 In A, C and E (first column) we have plotted daily confirmed cases \(C\) derived from the model (2.1) and it represents the first wave (A), beginning of the second wave (C) and a complete second wave (E), respectively. In B, D and F (second column) we have plotted \(\frac{dC}{dt}\) and we counted the number of sign changes (red circle) in the time series of \(\frac{dC}{dt}\). (Colour figure online)

2.3 Data

Daily COVID-19 confirmed cases for the six Indian states Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB) were collected [21] for the time period March 14, 2020, to May 12, 2021. State-wise demographic data were obtained from [37,58].

2.4 Estimation of parameters

Several Model (2.1) parameters are estimated (see Table 1) for the mentioned seven locations using daily confirmed COVID-19 cases. An elaboration of the estimation procedure is discussed in [49,50].

2.5 Basic reproduction number

The basic reproduction number \(R_0\) for the basic COVID-19 model (2.1) has the following expression (see Supplementary Appendix):

\[
R_0 = \frac{\chi \sigma \beta}{(\mu + \sigma)(\mu + \gamma_1)} + \frac{(1 - \chi) \sigma \beta}{(\mu + \sigma)(\mu + \gamma_2 + \tau)}.\]

(2.2)

To distinguish the transmission occurring from community, home-quarantined, symptomatic, asymptomatic infected population, we define the following reproduction numbers:

- Asymptomatic community reproduction number \(R^C_A\):

\[
R^C_A = \frac{\sigma \beta (\mu + \omega)}{(\mu + \sigma) [\mu + \omega + (1 - \theta)l]} \frac{\chi \rho}{(\mu + \gamma_1)}.\]

(2.3)

- Symptomatic community reproduction number \(R^C_S\):

\[
R^C_S = \frac{\sigma \beta (\mu + \omega)}{(\mu + \sigma) [\mu + \omega + (1 - \theta)l]} (1 - \chi) \frac{1 - \gamma_2 + \tau}{(\mu + \gamma_2 + \tau)}.\]

(2.4)

- Asymptomatic home-quarantined reproduction number \(R^H_A\):

\[
R^H_A = \frac{\sigma \beta (1 - \theta) l}{(\mu + \sigma) [\mu + \omega + (1 - \theta)l]} \frac{\chi \rho}{(\mu + \gamma_1)}.\]

(2.5)

- Symptomatic home-quarantined reproduction number \(R^H_S\):

\[
R^H_S = \frac{\sigma \beta (1 - \theta) l}{(\mu + \sigma) [\mu + \omega + (1 - \theta)l]} \frac{(1 - \chi)}{(\mu + \gamma_2 + \tau)}.\]

(2.6)

It can be easily verified that \(R_0 = R^C_A + R^C_S + R^H_A + R^H_S\).

2.6 Exploring multiple COVID-19 waves

One of the main aims of this study is to identify which model (2.1) parameters are most influencing on the
multiple waves in the dynamics of COVID-19 in these six states. To explore more on this, we carried out Sobol global sensitivity analysis [25,55] of these parameters with the number of COVID-19 waves during a time period \( W_C \) and the average number of cases in a wave \( A_W \). We derived \( W_C \) for a particular duration of the epidemic by counting the number of sign changes in the rate of change of daily confirmed cases \( C \). In Fig. 2A, time series of the daily confirmed cases \( C \) shows the first wave and \( \frac{dC}{dt} \) (see Fig. 2B) suggest one sign change. Similarly, the time series of the daily confirmed cases \( C \) in Fig. 2C suggests completion of the first wave and starting of the second wave. Corresponding in Fig. 2D suggests two sign changes in the time series of \( \frac{dC}{dt} \). Finally, Fig. 2E depicts completion of the second wave, and Fig. 2F shows three sign changes in the time series of \( \frac{dC}{dt} \). Sign changes of the time series in \( \frac{dC}{dt} \) in Fig. 2 lead us to develop the algorithm to compute \( W_C \) as follows:

- To neglect some initial fluctuations, we remove first 20 time points of the daily confirmed cases \( C \) simulation obtained from the COVID-19 model (2.1).
- If \( \text{sign change} = 1 \), then the first wave of the COVID-19 will be observed within the time period and therefore \( W_C = 1 \).
- If \( 2 \leq \text{sign change} \leq 3 \), then the second wave of the COVID-19 will be observed within the time period and therefore \( W_C = 2 \).
- If \( 4 \leq \text{sign change} \leq 5 \), then the third wave of the COVID-19 will be observed within the time period and therefore \( W_C = 3 \).
- If \( 6 \leq \text{sign change} \leq 7 \), then the fourth wave of the COVID-19 will be observed within the time period and therefore \( W_C = 4 \).
- This process will be continued for further waves of COVID-19.

Finally, the average number of cases in a wave \( A_W \) is computed using the following formula:

\[
A_W = \frac{\text{Total cases within a time period}}{W_C} \quad (2.7)
\]

2.7 Global sensitivity analysis

We determine the first-order \( (S_i) \) and total order \( (S_T) \) Sobol sensitivity index [25,55] of the parameters. Average transmission rate of symptomatic COVID-19 infected \( (\beta) \), Transmission variability factor between symptomatic and asymptomatic infection \( (\rho) \), Awareness response intensity \( (\psi) \), Fraction of home-quarantined population who maintain social distancing \( (\theta) \), Period of natural immunity in COVID-19 \( (\frac{1}{\omega}) \), Fraction of asymptomatic infected in the population \( (\chi) \), and Average notification rate \( (\tau) \) with responses the number of COVID-19 waves during a time period \( W_C \) and the average number of cases in a wave \( A_W \), respectively. We prefer to use global sensitivity based on Sobol indices as the responses \( W_C \) and \( A_W \) have a nonlinear non-monotone relationship with the mentioned parameters.

2.8 Model with vaccination

To determine an optimal COVID-19 vaccination and media awareness strategy, we incorporate the effect of vaccination in our model. We assumed that at time \( t \), a fraction \( p(t) \) of the susceptible and home-quarantined population are vaccinated (2 doses of Covishield) with vaccine efficacy \( \xi \). Those vaccinated individuals in susceptible and home-quarantined compartments move to the recovered compartment. As vaccination may not be able to life-long immunity against COVID-19 [48], therefore, we assume vaccine-based immunity wanes at a rate \( \omega_{R} \). We considered the time-dependent rate of awareness response \( \psi(t) \) to optimize the awareness response. Based on these assumptions, the extension of the model (2.1) is given as follows:

\[
\frac{dS}{dt} = \Pi + \omega SL - IS - \mu S - p(t)\xi S - \frac{\beta SI S}{N - \theta SL - H}
\]
\[
\frac{dSL}{dt} = \frac{\psi(t)SM}{1 + M} - IS - \mu SL - \omega SL - p(t)\xi SL - \frac{\beta(1 - \theta)SL IS}{N - \theta SL - H} - \frac{\rho\beta(1 - \theta)SL IA}{N - \theta SL - H} + \omega_{R} R
\]
\[
\frac{dE}{dt} = \frac{\beta SI S}{N - \theta SL - H} - \frac{\rho\beta SI S}{N - \theta SL - H} + \frac{\beta(1 - \theta)SI S}{N - \theta SL - H} - \frac{\rho\beta(1 - \theta)SI IA}{N - \theta SL - H} - (\sigma + \mu)E,
\]
\[
\frac{dIA}{dt} = \frac{\chi\sigma E - (\mu + \gamma_{1})IA}{1 + \gamma_{2}},
\]
\[
\frac{dIS}{dt} = (1 - \chi)\sigma E - (\mu + \gamma_{2} + \tau)IS,
\]
\[
\frac{dH}{dt} = \tau IS - (\mu + \delta)H - (1 - \xi)\gamma_{2}H - \xi\gamma_{2}\lambda H
\]
\[
\frac{dR}{dt} = γ_1 I_A + γ_2 I_S + (1 - \xi)γ_2 H + \xi γ_2 λ H + p(t) ζ (S + S_L) - (ω_r + μ) R
\]
\[
\frac{dM}{dt} = \frac{a H}{1 + H} - dM
\]  
(2.8)

2.9 Optimal cost-effectiveness strategy

One of the focuses of this study is to reduce COVID-19 cases at a minimum implementation cost of vaccination and awareness campaigns. In India, the first phase of vaccination started on January 16, 2021 [10]. However, in our COVID-19 model (2.8), we have considered the effect of full vaccination (a person received two doses of COVID-19 vaccine). The second dose of vaccination is started in India on February 13, 2021 [51]. Therefore, we carried out optimal vaccination effects from February 13, 2021, to August 31, 2021. However, the effect of awareness was studied from March 14, 2020, up to August 31, 2021. The difference in an awareness campaign with vaccination coverage is that the media campaign started as soon as the COVID-19 cases were observed in the country. To attain this goal, we constructed the following objective function:

\[
J(p(t), ψ(t)) = \int_{0}^{T_{\text{max}}} [A_1 δ H + A_2 ψ^4(t) + A_3 (\frac{R}{N})^m p^2(t) ζ] \, dt,
\]  
(2.9)

where \(A_1, A_2,\) and \(A_3\) are provided in Table 2. The first integrand in (2.9) represents the cost of COVID-19-related deaths [49]. The second integrand represents cost incurred in the process of information transmission [30]. The third integrand represents cost of vaccination [26].

We aim to minimize \(J\) with respect to vaccination rate \(p(t)\) and awareness response rate \(ψ(t)\) using Pontryagin’s maximum principle [30,49]. The minimization technique of the objective function \(J\) is discussed in Supplementary Appendix. We determine the daily average awareness response rate \(\hat{ψ}\) (from March 14, 2020, up to August 31, 2021), the daily average vaccination rate \(\hat{p}\) (from February 13, 2021, up to August 31, 2021), and the total vaccination coverage \(\hat{p}_T\) (from February 13, 2021, up to August 31, 2021) in six locations (AP, KA, KL, MH, TN, and WB) using the following formulae:

\[
\hat{ψ} = \frac{\int_{0}^{T_{\text{max}}} ψ(t) \, dt}{T_{\text{max}}},
\]
\[
\hat{p} = \frac{\int_{0}^{T_{\text{max}}} p(t) \, dt}{T_{\text{max}}},
\]  
(2.10)
\[
\hat{p}_T = \frac{\int_{0}^{T_{\text{max}}} p(t) ζ (S + S_L) \, dt}{\int_{0}^{T_{\text{max}}} (S + S_L) \, dt} \times 100.
\]

3 Results

Model (2.1) fitting to the daily COVID-19 cases from the six locations, namely Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB) for the time period March 14, 2020, to May 12, 2021, is provided in Fig. 3. It is clear from Fig. 3 that the basic COVID-19 model (2.1) can capture the trend of the second waves of COVID-19 cases in those six locations quite well. The estimated value of the symptomatic transmission rate \(β\) and variability factor between symptomatic and asymptomatic disease transmission \(ρ\) suggest that the severity of asymptomatic transmission is around 10% to 30% of the symptomatic transmission in all the six locations (see Table 3). Estimate of the fraction of home quarantined population who maintain social distancing, \(θ\) (see Table 3), suggests that in all six locations, about 1% to 4% of the total population under lockdown may contribute to new COVID-19 infection. Furthermore, the estimate of the percentage of asymptomatic infected \(χ\) was found to be higher than the percentage of symptomatic infected (see Table 3) in three locations, namely AP, MH, and WB, respectively. This suggests that the majority of COVID-19 cases in these three locations were undetected. Opposite trends were observed in KA, KL and TN, respectively. The recovery modification factor \(λ\) in all the six locations was less than unity (see Table 3). Therefore, our result indicates that hospitalized patients have a slower recovery rate compared to the natural recovery rate of the community symptomatic infected persons \(γ_2\) in five locations AP, KL, MH, TN, and WB, respectively (see Table 3).

Estimate of different reproduction numbers, \(R_{A}^{C}\) (asymptomatic community reproduction number), \(R_{S}^{C}\) (symptomatic community reproduction number), \(R_{A}^{H}\) (asymptomatic home quarantined reproduction number), \(R_{S}^{H}\) (symptomatic home quarantined reproduction number)
Table 2  Different cost coefficients

| Cost-coefficients parameters | Biological meaning                                                                 | Value     | References |
|-----------------------------|------------------------------------------------------------------------------------|-----------|------------|
| $A_1$                       | Cost of productive time lost per premature death due COVID (Calculated with life expectancy 73 years) (in USD) | 15,500    | [11]       |
| $A_2$                       | Average per day cost due to carry the COVID-19 awareness campaign (in USD)          | 847.9655  | [17]       |
| $A_3$                       | Two dose of Covishield (in USD)                                                    | 10.92     | [52]       |
| $m$                         | Quadratic correction term                                                           | 10        | [26]       |

Fig. 3  Model (2.1) to the daily COVID-19 cases from six states in India for the time period March 14, 2020, to May 12, 2021. Observed cases are in blue circle, and black line is the model solution. Here, subscripts AP, KA, KL, MH, TN, and WB are Andhra Pradesh, Karnataka, Kerala, Maharashtra, Tamil Nadu, and West Bengal, respectively

Transmission number), and $R_0$ (the basic reproduction number), suggested that COVID-19 transmission dominated by the community infection (see Table 4). This result is consistent with the fact that only 1% to 4% percentage of home quarantined population may contribute to new COVID-19 infection (see estimate of $\theta$ in Table 3). In WB community, infection is dominated by asymptomatic infection ($R^A_C > R^S_C$), whereas in other five locations (AP, KA, KL, MH, and TN) community, symptomatic infection is dominating (see Table 4). Opposite trend observed in WB is due to higher percentage of asymptomatic infection in the population (see value of $\chi$ in Table 3) and higher value of the transmission variability between symptomatic and asymptomatic (see value of $\rho$ in Table 3).

Three key parameters that mainly influence (value of the total order Sobol sensitivity index) the number of COVID-19 waves ($W_C$) in all six locations (AP, KA, KL, MH, TN, and WB) are the average transmission rate of symptomatic COVID-19 infected ($\beta$), the average notifications & hospitalization rate ($\tau$) and the variability in transmission between symptomatic and asymptomatic ($\rho$) [see Fig. 4]. Similar to $W_C$, the average number cases in a COVID-19 waves ($A_W$) mainly influenced by $\beta$ (see Fig. 5). Furthermore, other parameters like $\theta$ (fraction of home-quarantined population
Table 3 Estimated parameters (95% CI) of the mechanistic mathematical model (2.1) for the six locations Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB), respectively

|     | AP               | KL               | MH               | TN               | WB               |
|-----|------------------|------------------|------------------|------------------|------------------|
| $\beta$ | 1.084 (0.9974–1.3954) | 1.4650 (1.3194–1.4834) | 0.6715 (0.4931–1.1352) | 1.0518 (1.0663–1.6046) | 1.3095 (1.2039–1.3540) | 1.1823 (1.2870–2.0554) |
| $\rho$ | 0.1052 (0.1001–0.1204) | 0.1048 (0.1008–0.1554) | 0.1961 (0.1013–0.2872) | 0.1334 (0.1005–0.1661) | 0.1139 (0.1013–0.1518) | 0.1473 (0.1004–0.1850) |
| $\psi$ | 0.0997 (0.9209–0.9998) | 0.9866 (0.9557–0.9996) | 0.6808 (0.5777–0.7202) | 0.7130 (0.4872–0.7716) | 0.9962 (0.9745–0.9998) | 0.9796 (0.9272–0.9994) |
| $\theta$ | 0.9726 (0.9680–0.9755) | 0.9998 (0.9988–0.9999) | 0.9933 (0.9922–0.9999) | 0.9990 (0.9971–0.9999) | 0.9998 (0.9992–0.9999) | 0.9999 (0.9998–0.9999) |
| $\omega$ | 0.0042 (0.0041–0.0043) | 0.0042 (0.0041–0.0043) | 0.01554 (0.01364–0.01636) | 0.0070 (0.0063–0.0076) | 0.0045 (0.0041–0.0049) | 0.0077 (0.0073–0.0083) |
| $\chi$ | 0.7198 (0.6604–0.7739) | 1.285E–3 (1.04E–3–6.608E–3) | 9.01E–3 (1.41E–3–0.0508) | 0.6927 (0.6904–0.7701) | 3.0E–3 (1.055E–3–0.01033) | 0.7769 (0.7770–0.8256) |
| $\tau$ | 0.1807 (0.1471–0.2810) | 0.9851 (0.88–0.9985) | 0.4093 (0.2594–0.7678) | 0.1889 (0.1486–0.3715) | 0.9657 (0.8806–0.9989) | 0.4197 (0.2680–0.6438) |
| $\lambda$ | 0.1966 (0.0043–1.4272) | 0.09133 (0.0048–0.3525) | 0.1722 (0.0086–1.4828) | 0.3499 (0.0052–1.6119) | 0.1834 (0.00194–0.2817) | 0.8481 (0.01485–1.6156) |
| $l$ | 0.042 (0.017–0.8782) | 0.7350 (0.0114–0.8244) | 0.8385 (0.05258–0.8942) | 0.7257 (0.0511–0.8824) | 0.3122 (0.012–0.7847) | 0.7437 (0.04406–0.8902) |
Table 4  Estimated values of the community ($R_C^A$ and $R_C^S$), the home-quarantined ($R_H^A$ and $R_H^S$), and the basic ($R_0$) reproduction numbers for Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maharashtra (MH), Tamil Nadu (TN), and West Bengal (WB). All data are given in the format [Mean(95% CI)]

| Location         | $R_C^A$ (Mean(95% CI)) | $R_H^A$ (Mean(95% CI)) | $R_C^S$ (Mean(95% CI)) | $R_H^S$ (Mean(95% CI)) | $R_0$ (Mean(95% CI)) |
|------------------|------------------------|------------------------|------------------------|------------------------|----------------------|
| Andhra Pradesh (AP) | 0.4732 (0.2532–0.8075) | 0.2751 (0.0266–0.5260) | 0.7582 (0.4341–1.1918) | 0.4529 (0.0394–0.80)   | 1.9595 (1.7876–2.1151) |
| Karnataka (KA)   | 0.0036 (0.0013–0.0090) | 1.74E−5 (1.38E−07 - 1.23E−4) | 1.3963 (1.3540–1.4135) | 0.0068 (7.31E−5–0.05196) | 1.4068 (1.3946–1.4186) |
| Kerala (KL)      | 0.015 (0.0011–0.05632) | 1.5E−4 (4.44E−7–9.04E−4)  | 1.4255 (1.33–1.5286) | 0.0127 (1.6E–4–0.0513) | 1.4534 (1.3697–1.5489) |
| Maharashtra (MH) | 0.8691 (0.6224–1.222)  | 0.0236 (3.89E−4–0.0869)  | 1.1821 (0.8345–1.466) | 0.0329 (4.79E–4–0.1223) | 2.108 (2.012–2.2194)   |
| Tamil Nadu (TN)  | 0.0043 (0.0013–0.0129) | 1.74E−5 (7.20E−8–1.13E−4) | 1.2729 (1.2450–1.2854) | 0.0053 (3.0E–5–0.0318) | 1.2827 (1.2754–1.29)   |
| West Bengal (WB) | 1.2592 (0.9716–1.6394) | 0.0032 (4.89E−5–0.0127)  | 0.7014 (0.4129–0.9546) | 0.0020 (2.58E–5–0.0083) | 1.9658 (1.889–2.08)    |
Fig. 4 The first-order and total order Sobol sensitivity index of some of the model (2.1) parameters with number COVID-19 waves ($W_C$) during the time period March 14, 2020, to May 12, 2021.

Fig. 5 The first-order and total order Sobol sensitivity index of some of the model (2.1) parameters with average number COVID-19 cases in a wave ($A_W$) for the time period March 14, 2020, to May 12, 2021.
who maintain proper social distancing), \( \omega_r \) (rate of loss of natural immunity of COVID-19), \( \chi \) (average fraction of the COVID-19 exposed population that become asymptotic infected) and \( \tau \) also have similar impact on \( A_W \) (see Fig. 5). Therefore, policymakers should focus on controlling these six parameters (\( \beta, \tau, \rho, \theta, \omega_r, \) and \( \chi \)) to restrict further COVID-19 waves and reduce number of cases in a wave in these six locations, namely MH, TN, KA, KL, AP, and WB.

Optimal effect of the interventions vaccination, awareness and their combination are compared in terms of cases reduction (see Table 5) and also total implementation cost (see Table 8). In Table 5, base cases are projected for the period March 14, 2020, to August 31, 2021, for six locations MH, KL, TN, AP, WB, and KA using the basic COVID-19 model (2.1) (with fixed awareness rate \( \psi \)). Optimal cases based on interventions, namely only vaccination (VA), only media awareness (ME), and combination of vaccination & media (VA+ME), are projected for the time period March 14, 2020, to August 31, 2021, for the mentioned six locations (see Table 5). Optimal vaccination effects (VA and VA+ME) are studied from February 13, 2021, onwards in these mentioned six locations. This is because India’s second dose of vaccination (Covishield) started on February 13, 2021. Our result suggests that only vaccination (without any awareness) is not at all effective in reducing COVID-19 cases in all locations.

### Table 5  Total number of COVID-19 cases from March 14, 2020, to August 31, 2021, under each intervention scenario at an optimal rate. Base cases indicate the number of COVID-19 cases during March 14, 2020, to August 31, 2021, predicted by the basic COVID-19 model (2.1). Fixed and estimated parameters used in calculating base cases are taken from Table 1 and 3.

|                | Maharashtra (MH) | Kerala (KL) | Tamil Nadu (TN) |
|----------------|------------------|-------------|-----------------|
| **Base cases** | 8.31E6 (8.13E6–8.48E6) | 5.53E6 (5.31E6–5.78E6) | 4.41E6 (4.28E6–4.53E6) |
| VA             | 2.05E7 (1.84E7–2.41E7) | 1.90E7 (1.84E7–1.95E7) | 3.25E7 (3.17E7–3.36E7) |
| ME             | 5.66E6 (4.86E6–6.86E6) | 4.40E6 (4.15E6–4.68E6) | 3.14E6 (2.92E6–3.40E6) |
| VA+ME          | 2.65E6 (1.92E6–3.70E6) | 6.92E5 (6.30E5–7.54E5) | 5.59E6 (4.24E6–6.60E6) |

|                | Andhra Pradesh (AP) | West Bengal (WB) | Karnataka (KA) |
|----------------|---------------------|------------------|----------------|
| **Base cases** | 2.56E6 (2.39E6–2.78E6) | 2.99E6 (2.86E6–3.14E6) | 5.21E6 (5.04E6–5.36E6) |
| VA             | 8.17E6 (6.79E6–1.02E7) | 1.24E7 (1.16E7–1.33E7) | 3.19E7 (3.04E7–3.36E7) |
| ME             | 1.98E6 (1.83E6–2.18E6) | 3.01E6 (2.84E6–3.16E6) | 2.42E6 (2.08E6–2.81E6) |
| VA+ME          | 2.07E6 (1.75E6–2.41E6) | 7.92E5 (7.0E5–1.05E6) | 6.32E6 (4.11E6–7.59E6) |

### Table 6  Estimates of the average optimal rates of vaccination (during February 13, 2021, to August 31, 2021) and the average awareness response intensity (during March 14, 2020, to August 31, 2021) for six locations AP, KA, KL, MH, TN, and WB under three intervention scenarios. Here, VA-vaccination, ME-media, and VA+ME-combination of vaccination & awareness.

|                | Maharashtra (MH) | Kerala (KL) | Tamil Nadu (TN) |
|----------------|------------------|-------------|-----------------|
| VA \((p)\)     | 0.1216 (0.1142–0.1290) | 0.088 (0.0798–0.1024) | 0.0092 (0.0076–0.0136) |
| ME \((\psi)\)  | 0.7753 (0.7564–0.7973) | 0.6557 (0.6498–0.6621) | 0.4265 (0.4110–0.4361) |
| VA+ME \((p)\)  | 0.0152 (0.0047–0.049) | 0.0519 (0.0416–0.0620) | 0.0020 (0.0019–0.0023) |
| VA+ME \((\psi)\) | 0.4054 (0.3988–0.4138) | 0.3202 (0.3158–0.3279) | 0.2056 (0.1921–0.2158) |

|                | Andhra Pradesh (AP) | West Bengal (WB) | Karnataka (KA) |
|----------------|---------------------|------------------|----------------|
| VA \((p)\)     | 0.0648 (0.0613–0.0694) | 0.1190 (0.11–0.1249) | 0.0306 (0.0230–0.0389) |
| ME \((\psi)\)  | 0.7599 (0.7204–0.7910) | 0.7122 (0.7018–0.7296) | 0.8021 (0.7676–0.8219) |
| VA+ME \((p)\)  | 0.0061 (0.0034–0.0113) | 0.0699 (0.0446–0.0861) | 0.0036 (0.0019–0.0063) |
| VA+ME \((\psi)\) | 0.3859 (0.3695–0.4081) | 0.2762 (0.2664–0.2815) | 0.3854 (0.3801–0.3898) |
Table 7  Estimates of the optimal vaccination coverage during the period February 13, 2021, to August 31, 2021, under two lockdown scenarios (VA and VA+ME) in the locations AP, KA, KL, MH, TN and WB

| Location         | Vaccination (VA) only (%) | Combination (VA+ME) (%) |
|------------------|---------------------------|-------------------------|
| Maharashtra (MH) | 44.24% (43.25–45.16%)     | 35.38% (30.70–42.88%)   |
| Kerala (KL)      | 31.45% (30.43–33.53%)     | 33.45% (31.24–35.95%)   |
| Tamil Nadu (TN)  | 34.87% (33.56–37.37%)     | 26.41% (25.89–27.79%)   |
| Andhra Pradesh (AP) | 43.22% (42.33–43.80%) | 38.68% (30.50–44.52%)   |
| West Bengal (WB) | 41.31% (40.54–42.12%)     | 43.65% (40.52–45.35%)   |
| Karnataka (KA)  | 41.06% (39.02–42.34%)     | 27.10% (25.64–43.89%)   |

Table 8  Costs (in USD) of optimal interventions under different control scenarios (VA, ME, and VA+ME) at different optimal rates. Costs of vaccination (VA) and media awareness (ME) are measured for the time period February 13, 2021, up to August 31, 2021, and March 14, 2020 up to August 31, 2021, respectively.

| Location         | VA (USD) (95% CI) | ME (USD) (95% CI) | VA+ME (USD) (95% CI) |
|------------------|------------------|------------------|----------------------|
| Maharashtra (MH) | 2.13E8 (1.85E8–2.54E8) | 5.41E7 (4.61E7–6.68E7) | 2.80E7 (2.04E7–4.01E7) |
| Kerala (KL)      | 4.01E7 (3.54E7–4.27E7) | 8.52E6 (7.42E6–9.38E6) | 1.59E6 (1.34E6–1.78E6) |
| Tamil Nadu (TN)  | 1.24E6 (1.19E6–1.29E6) | 2.06E5 (1.92E5–2.14E5) | 2.48E5 (1.80E5–2.93E5) |

| Andhra Pradesh (AP) | VA (USD) (95% CI) | ME (USD) (95% CI) | VA+ME (USD) (95% CI) |
|---------------------|------------------|------------------|----------------------|
|                     | 3.88E7 (3.18E7–4.89E7) | 1.04E8 (9.03E7–1.16E8) | 9.86E6 (8.36E6–1.13E7) |
| West Bengal (WB)    | 1.04E8 (9.03E7–1.16E8) | 2.35E7 (2.06E7–2.54E7) | 9.45E6 (8.46E6–1.10E7) |
| Karnataka (KA)      | 2.29E8 (2.12E8–2.43E8) | 1.75E7 (1.48E7–2.05E7) | 4.53E7 (2.95E7–5.35E7) |

six states (see Table 5). The optimal effect of media awareness (ME) (see Table 5, and Table 8) is found to be most cost-effective (in terms of implementation cost and cases reduction) in AP (about 22% reduction from the base cases), TN (about 29% reduction compared to base cases) and KA (about 54% reduction compared to base cases). In KL, and MH, awareness is also found to have a significant impact (about 20% to 30% reduction from the base cases) in cases reduction (see Table 5). Applying only media awareness (ME) is not found to be effective in WB in terms of cases reduction. Optimal awareness & vaccination combination (VA+ME) found to be most cost-effective (in terms of implementation cost and cases reduction) in MH (about 97% reduction from the base cases), KL (about 87% reduction from the base cases), and WB (about 74% reduction from the base cases) [see Table 5]. In Tables 6 and 7, we have provided average optimal rates at which awareness campaigns and vaccination may be carried out in the six locations MH, KL, TN, AP, WB, KA, respectively. Our results suggest that a large percentage of the population (26% to 45%) must be vaccinated from February 13, 2021, to August 31, 2021, in order to avert an optimal number of COVID-19 cases in these six locations (see Table 7).

4 Discussion

In this paper, we considered a new COVID-19 mathematical model (2.1) with imperfect lockdown effect, reinfection of recovered COVID-19 cases, and media awareness. We have analyzed the invariance and boundedness of the solution. The local asymptotic stability of the disease-free equilibrium (DFE) has been studied analytically with the help of the next-generation matrix technique. Due to the high nonlinearity of the model, we have analyzed the model numerically to find all possible equilibrium points and studied their local stability analysis. Several parameters are estimated by the fitting solution of the model (2.1) to daily notified cases for the time period March 14, 2020, till May 12, 2021, from six states, namely Andhra Pradesh (AP), Karnataka (KA), Kerala (KL), Maha-
rashtra (MH), Tamil Nadu (TN), and West Bengal (WB), respectively. We estimated (see Table 4) the community (symptomatic and asymptomatic) reproduction number ($R^C_S$ and $R^C_A$), the home quarantined (symptomatic and asymptomatic) reproduction number ($R^H_S$ and $R^H_A$), the basic reproduction number ($R_0$) for the six mentioned states, respectively. To determine a relationship between model (2.1) parameters with the number of COVID-19 waves ($W_C$) and the average number of notified cases in a wave ($A_W$), we develop an algorithm to count the number of waves and the average notified cases for the six location from the solution of the model (2.1). Using this algorithm, we perform a variance-based global sensitivity analysis based on Sobol’s method of seven key epidemiological parameters of the model (2.1) with two responses, namely $W_C$ and $A_W$, respectively. Moreover, the model (2.1) is then extended to carry out an optimal cost-effective study of some important COVID-19 control strategies (awareness, vaccination, and their combination) in terms of cases reduction and their implementation cost. Our results suggest that a negligible percentage (about 1% to 4%) of COVID-19 transmission occurs from the home-quarantined population. Thus, in these six states, COVID-19 transmission is dominated by community infection. Our analysis suggest that the asymptomatic transmission is less severe (approximately 10% to 30% of the average symptomatic transmission rate) than the symptomatic transmission (see Table 3) in all six locations. This result also reflected in the estimation of community ($R^C_A$, and $R^C_S$) and home-quarantined ($R^H_A$, and $R^H_S$) reproduction numbers. Results on global sensitivity analysis of model parameters suggest that $\beta$, $\tau$, and $\rho$ are mainly influence the number of COVID-19 waves in the six locations. Optimal use of vaccination and media awareness will reduce the effect of $\beta$ and $\rho$. Furthermore, rapid COVID-19 testing will reduce the effect of $\tau$. Therefore, policymakers may focus on controlling these parameters to control future COVID-19 waves and the average number of cases in a wave. The optimal cost-effective study suggests that awareness as a single intervention and awareness with a combination of vaccination are the two best control strategies in terms of case reduction and implementation cost. In the case of control combination (media awareness and vaccination), a large percentage of the population must be vaccinated in order to reduce the significant number of COVID-19 cases in the mentioned six locations.

Finally, we discuss some drawbacks of the present study and may be extended in from diverse perspectives. In the COVID-19 system (2.1), we assumed that home-quarantined (due to awareness and lockdown) individuals are all susceptible. However, it is possible that a home-quarantined individuals can be COVID-19 exposed or symptomatic or asymptomatic. Consequently, In our study, we neglect the possibility of cross-infection between different home-quarantined population. Furthermore, in this current manuscript, we have shown analytically local asymptotic stability of the DFE ($E_0$) [see Supplementary Appendix], and also numerically shown the existence and stability of the endemic equilibrium point of the model (2.1) in terms of the basic reproduction number ($R_0$). However, we have yet to determine the full analytical stability of the endemic equilibrium point of the COVID-19 model (2.1). We shall explore these challenging problems in our future studies.

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Data availability The authors declare that all data generated or analyzed during this study are included in this article.

Declarations

Conflict of interests The authors declare that they have no conflicts of interest.

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