Searching for solar axions at the Sudbury Neutrino Observatory

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We explore a novel detection possibility for solar axions, which relies only on their couplings to nucleons, via the axion-induced dissociation of deuterons into their constituent neutrons and protons. An opportune target for this process is the now-concluded Sudbury Neutrino Observatory (SNO) experiment, which relied upon large quantities of heavy water to resolve the solar neutrino problem. From the full SNO dataset we exclude in a model-independent fashion isovector axion-nucleon couplings $|g_{aN}^{3}| \equiv \frac{1}{2}|g_{AN} - g_{ap}| > 2 \times 10^{-5}\text{GeV}^{-1}$ at 95 \% C.L. for sub-MeV axion masses, covering previously unexplored regions of the axion parameter space. In the absence of a precise cancellation between $g_{AN}$ and $g_{ap}$ this result also exceeds comparable constraints from other laboratory experiments, and excludes regions of the parameter space for which astrophysical constraints from SN1987A and neutron star cooling are inapplicable due to axion trapping.

\textbf{Introduction.} Arising straightforwardly as a minimal extension of the Standard Model, and in particular the Peccei-Quinn solution of the strong CP problem \cite{1–3}, axions and axion-like particles (ALPs) occupy a rare focal point in theoretical physics, in that they are also simultaneously a generic prediction of the exotic physics of string and M-theory compactifications \cite{4, 5}. Despite the profound differences between these contexts the resulting axion properties are largely universal, creating an easily-characterisable theoretical target.

As typically light, long lived pseudoscalar particles they can also influence many aspects of cosmology and astrophysics, leading to a wealth of observational signatures \cite{6}. In particular, they provide a natural candidate for the mysterious dark matter comprising much of the mass of our visible universe \cite{7, 8}, and as such are an focal point of intense ongoing investigation \cite{9}.

Fortuitously, our own Sun should provide an intense and readily available axion flux from which much of the corresponding parameter space can be constrained. At present the strongest resulting constraint is provided by the CAST experiment \cite{10}, which relies upon the Primakoff conversion of axions into photons in a background magnetic field. Presumably for reasons of observational and experimental convenience, most of the existing axion literature rests similarly on axion-photon interactions.

We will in the following instead turn attention to a less well-explored corner of the parameter space, and in particular the axion-nucleon interactions

$$\mathcal{L} = \frac{1}{2}g_{an}\partial_{\mu}a \gamma_{\mu} \gamma_{5} n + \frac{1}{2}g_{ap}\partial_{\mu}a \gamma_{\mu} \gamma_{5} p,$$

which can be re-expressed in terms of the neutron/proton doublet $N = (n, p)$ as

$$\mathcal{L} = \frac{1}{2}\partial_{\mu}a N \gamma_{\mu} \gamma_{5} \left( g_{aN}^3 I + g_{aN}^3 \tau_3 \right) N,$$

where the isoscalar and isovector couplings are respectively $g_{aN}^3 = (g_{an} + g_{ap})/2$, $g_{AN}^3 = (g_{AN} - g_{ap})/2$, and $\tau_3 = \text{diag}(1, -1)$. If required integration by parts can be used to recast this into

$$\mathcal{L} = -ia\overline{N} \gamma_5 m_N \left( g_{aN}^3 I + g_{aN}^3 \tau_3 \right) N,$$

where $m_N = \text{diag}(m_n, m_p)$.

There are comparatively few constraints on axion-nucleon interactions, arising primarily from considerations of SN1987A \cite{12–15} and neutron star (NS) observations \cite{16–19}, experimental searches for new spin-dependent forces \cite{20, 26} and time dependent nuclear electric dipole moments \cite{27}. It should however be noted that the overall paradigm of axion constraints derived from SN1987A has been called into question \cite{28, 29}.

The CASPER experimental program is also searching for axion dark matter via nuclear interactions \cite{30, 32}, and similar considerations have led recently to novel constraints from existing comagnetometer data \cite{33}.

Limits also exist from rare meson decays \cite{34} and dedicated solar axion experiments which rely only upon nuclear couplings \cite{35, 40}, however as these are model-dependent we will not consider them going forward.

As we will demonstrate, there is also an entirely novel and model-independent constraint arising from axions emitted during nuclear transitions inside the Sun, which can be detected on Earth through the M1 process

$$a + \delta \to n + p,$$

where $\delta$ is a deuteron. A particularly opportune target for this mechanism is the now-concluded Sudbury Neutrino Observatory (SNO) experiment, which relied upon a large quantity of deuterium to resolve the solar neutrino problem. The possibility of using deuterium for axion detection was first noted by Weinberg in \cite{2}.

After detailing the corresponding axion flux and interaction cross section for (4) in Sections 2 and 3, we will compute in Section 4 the resulting axion-induced event...
rate in SNO and derive constraints therefrom. Conclusions and discussion are presented in closing.

**Solar axion flux.** Whilst axions can in general be produced within stars by a number of processes, such as Primakoff conversion, electron bremsstrahlung and Compton scattering, we are primarily interested here in their production via low-lying nuclear transitions. This is primarily because the threshold for deuterium dissociation via (4) is 2.2 MeV, and so only solar axions arising from nuclear transitions will have sufficient energy. However there is also secondary benefit in so doing in that both emission and detection will rely only upon a single axion-nucleon coupling, allowing a model-independent constraint of general applicability.

Of the nuclear transitions occurring inside the sun, the most intense axion flux is provided by

\[ p + d \rightarrow ^3\text{He} + \gamma \text{(5.5MeV)} \]  

where an axion substitutes for the emitted gamma ray. In the Standard Solar Model (SSM) this constitutes the second stage of the pp fusion chain, with the first stage provided by the two reactions \( p + p \rightarrow d + e^+ + \nu_e \) and \( p + p + e^- \rightarrow d + \nu_e \). As the deuterons produced via this first stage capture protons within \( \tau \approx 6 \) s, the axion flux resulting from (5) can be expressed in terms of the known pp neutrino flux.

The constant of proportionality is the probability for a given M1 nuclear transition to result in axion rather than photon emission,

\[ \frac{\Gamma_a}{\Gamma_\gamma} \simeq \frac{1}{2\pi\alpha} \frac{m_n^2}{M} \left( \frac{\beta g_{aN} + g_{aN}^3}{(\mu_0 - 0.5) \beta + \mu_3 - \eta} \right)^2 \frac{p_0}{p_\gamma}^3, \]

where \( \alpha \) is the fine structure constant, \( \delta^2 = E/M \) is the relative probability for E and M transitions, we set \( m_n = m_p \), and \( \mu_0 = \mu_p + \mu_n \simeq 0.88 \) and \( \mu_3 = \mu_p - \mu_n \simeq 4.71 \) are respectively the isoscalar and isovector nuclear magnetic moments, and \( p_\alpha/p_\gamma \) are the axion/photon momenta [42]. Dependence on specific nuclear matrix elements enters through \( \beta \) and \( \eta \).

In [43], the M1-type transitions associated to axion emission correspond to capture of protons with zero orbital momentum. The probability of this occurring at a proton energy of 1 keV has been measured and found to be 0.55 [43], implying \( \delta^2 = 0.82 \). Since capture from the S state corresponds to an isovector transition, we can neglect the \( g_{aN}^1 \) contribution to (6) and, to a good approximation, also ignore everything other than \( \mu_3 \) in the denominator [44], leading to

\[ \frac{\Gamma_a}{\Gamma_\gamma} \simeq \frac{1}{2\pi\alpha} \frac{m_n^2}{M} \left( \frac{g_{aN}^3}{\mu_3} \right)^2 \left( \frac{p_0}{p_\gamma} \right)^3, \]

which ultimately provides the axion flux at Earth

\[ \phi_a \simeq 3.23 \times 10^{10} m_n^2 (g_{aN}^3)^2 \left( \frac{p_0}{p_\gamma} \right)^3 \text{cm}^{-2}\text{s}^{-1}. \]

As this component of the solar axion flux has already been well constrained by the Borexino and CAST experiments via a number of detection channels [45,46], we will in the following focus only on the previously unexplored detection channel provided by deuterium [4].

**Axiodissociation cross section** We now construct the cross section for the ‘axiodissociation’ process

\[ a + d \rightarrow n + p, \]

with threshold energy 2.2 MeV. For reasons of clarity and brevity we give a relatively simple derivation of this quantity, postponing more thorough study to the future. Details of the corresponding nuclear physics are found in [47,48].

Working in the rest frame of the initial state deuteron, the number of events we expect is

\[ N_e = \sigma \phi N_d T, \]

where \( \phi \) is the incoming flux, \( N_d \) the number of targets and \( T \) the time, we can rearrange for a single deuteron to give \( \sigma = (V/v_i)(N_e/T) \), where we have used the fact that for a single incoming axion \( \phi \equiv n_i = v_i/V \). No integration over energy is required since thermal broadening is negligible relative to the axion energy at hand.

Identifying \( N_e/T \) as the transition rate per unit time, we can make use of Fermi’s golden rule to write

\[ \sigma = \frac{2\pi V}{v_i} |\langle f|H_I|i\rangle|^2 \rho(k), \]

where the initial and final states are

\[ |i\rangle = ^3S_1; q, \quad |f\rangle = ^1S_0; 0 \],

a deuteron in the \(^3S_1\) ground state and an incoming axion, and a deuteron in the \(^1S_0\) first excited state, while (2) gives the non-relativistic interaction Hamiltonian

\[ H_I \simeq \frac{1}{2} \left( g_{aN}^1 I + g_{aN}^3 \tau_3 \right) \vec{a} \cdot \vec{\sigma}. \]

We can expand in momentum modes via

\[ a(x) = \frac{1}{\sqrt{V}} \int dp \frac{1}{\sqrt{2E'}} \left( a(q') e^{iq'\cdot x} + a^\dagger(q') e^{-iq'\cdot x} \right), \]

so that due to the raising operation \( \langle 0|a(q') = \langle q'| \), the axion part of the matrix element contains \( \langle 0|a(q')|q \rangle = \delta_{qq'} \), which removes the summation over modes. Taking the derivative to get a factor of \( q \), we then have

\[ \langle f|H_I|i\rangle \equiv \frac{i}{\sqrt{8E_qV}} \langle ^1S_0| \left( g_{aN}^1 I + g_{aN}^3 \tau_3 \right) \vec{q} \cdot \vec{\sigma} e^{iq\cdot x} | ^3S_1 \rangle, \]

where the exponential factor can be neglected as a long-wavelength approximation. To account for the isospin structure we can rewrite

\[ (g_{aN}^1 I + g_{aN}^3 \tau_3) \vec{\sigma} = g_{aN}^1 (\vec{\sigma}_n + \vec{\sigma}_p) + g_{aN}^3 (\vec{\sigma}_n - \vec{\sigma}_p), \]

where the first term gives zero action on the outgoing singlet state, since in that case the neutron and proton spins are anti-aligned, so that we then have

\[ \langle f|H_I|i\rangle = \frac{i|q|g_{aN}^1}{\sqrt{8E_qV}} \langle ^1S_0| \vec{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p) | ^3S_1 \rangle. \]
To evaluate this expression fully, we need to solve the Schrödinger equation for the deuteron wavefunction. Although in principle a two-body problem, we can reduce this to a one-body problem satisfying

$$\frac{1}{2m} \frac{\partial^2}{\partial r^2} (r \psi(r)) + (E_D - V(r)) \psi(r) = 0,$$

(18)

where $m \approx m_n/2$ is the reduced mass, $r$ is the distance between nucleons, $E_D = 2.2$ MeV the binding energy of the deuteron and $\psi$ and $V$ are functions of $r$ only due to the spherical symmetry of the presumed $S$-wave ground state. For the simplest possible approximation we can take $V_0$ corresponding to a delta function potential at the origin, which then yields

$$\psi_3 = \frac{1}{\sqrt{4\pi r^2}} u(r) \chi_3, \quad u(r) = Ne^{-ar},$$

(19)

where $N = \sqrt{2\pi}$ and $a = \sqrt{m_n E_D}$, which satisfies the normalisation condition $\langle \psi | \psi \rangle = \int \psi^* \psi \, dV = 1$. The spin of the triplet is encoded in the eigenfunction

$$\chi_3^m = \left\{ \begin{array}{l} (|n^1 p^1\rangle, \quad S_z = +1) \\ \frac{1}{\sqrt{2}}(|n^1 p^1\rangle + |n^1 p^1\rangle), \quad S_z = 0 \\ \frac{1}{\sqrt{2}}(|n^1 p^1\rangle - |n^1 p^1\rangle), \quad S_z = -1 \end{array} \right.$$ (20)

where $S_z$ is the $z$ component of the spin.

The eigenfunction of the outgoing singlet is

$$\psi_0 = \frac{1}{\sqrt{4\pi r^2}} j(r) \chi_0, \quad j(r) = \sqrt{\frac{2}{L}} \sin(kr + \delta_0),$$

(21)

where $\delta_0$ is the $s$-wave phase shift produced by the singlet potential and $\chi_0 = \frac{1}{\sqrt{2}}(|n^1 p^1\rangle - |n^1 p^1\rangle)$. With the boundary condition $kL + \delta_0 = n\pi$ it is straightforward to check that $\int |\psi_0|^2 dV \to 1$ as $L \to \infty$. We can then write

$$\langle 1^S_0 | \hat{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p) | 3^S_1 \rangle = \int j(r)^* u(r) \langle \chi_0, \hat{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p) \chi_3 \rangle \, dr,$$

(22)

where $(\psi, \chi)$ denotes the usual inner product for spinors. For the $r$-dependent piece we have

$$\int j(r)^* u(r) \, dr = \sqrt{\frac{2}{L}} N (\alpha \sin(\delta_0) + k \cos(\delta_0)) \frac{k^2}{k^2 + \alpha^2}.$$

(23)

We can further introduce the singlet scattering length $a_s = -1/k \cot(\delta_0) = -23.7$ fm, to yield

$$\int j(r)^* u(r) \, dr = \sqrt{\frac{2}{L}} Nk(1 - \alpha a_s) \frac{k^2 \sqrt{1 + k^2 a_s^2}}{(k^2 + \alpha^2)^3/2}.$$ (24)

The spin-dependent factor in $|\langle f | H_2 | i \rangle|^2$, given that we must average over all the incoming deuteron polarisations, is $\frac{1}{3} \sum_m |\langle \chi_0, c \cdot (\vec{\sigma}_n - \vec{\sigma}_p) \chi_3^m \rangle|^2$, where we sum over all possible spin states of the triplet ground state. Considering the $z$ component of $\vec{\sigma}$ acting on the spin-dependent part of the wavefunction, $\sigma_z \uparrow = \uparrow \uparrow$ and $\sigma_z \downarrow = -\downarrow \downarrow$ so that for the singlet state of the deuteron we have

$$(\sigma_n - \sigma_p)^2 \frac{1}{\sqrt{2}}(|n^1 p^1\rangle - |n^1 p^1\rangle) = \frac{2}{\sqrt{2}}(|n^1 p^1\rangle + |n^1 p^1\rangle),$$

(25)

which is twice the $S_z = 0$ eigenfunction for the incoming $^3S_1$ state. As this implies $\langle \chi_0, (\vec{\sigma}_n - \vec{\sigma}_p) | \chi_0 \rangle = 0$ we can extend the sum to cover all possible states and then rewrite the spin-dependent factor as

$$\frac{1}{3} \sum_m \langle \chi_0, \hat{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p) \chi_m \rangle \langle \chi_m, \hat{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p) | \chi_0 \rangle.$$ (26)

Recognising the insertion of $\sum_m |\chi_m \rangle \langle \chi_m | = 1$, this is

$$\frac{1}{3} \langle \chi_0, \hat{q} \cdot (\vec{\sigma}_n - \vec{\sigma}_p)^2 | \chi_0 \rangle = \frac{4}{3},$$

(27)

where we have used $\vec{\sigma}_n | \chi_0 \rangle = -\vec{\sigma}_p | \chi_0 \rangle$ and $\sigma_z | \chi_0 \rangle = \delta^z_j$. From the boundary condition $kL + \delta_0 = n\pi$ we have a single state for each $n$, so that the number of outgoing states between $k$ and $k + dk$ is

$$dn = \frac{1}{\pi} \left( L + \frac{dk}{dk} \right) dk.$$ (28)

Given that $dk/dE_k = 1/v_f$, from (11) we then have

$$\sigma = \frac{2VL}{v_f^2} |\langle f | H_2 | i \rangle|^2.$$ (29)

Using $\sqrt{q} = \gamma m_n a^2 v_i = E_a v_i$ and $|k| = \sqrt{m_n (E_a - E_D)}$,

$$\sigma = \frac{2}{3} (g_{aN})^2 m_n \sqrt{E_a^2 - m_n^2} \frac{|\vec{k}| \alpha (1 - \alpha a_s)^2}{(k^2 + \alpha^2)^3/2}.$$ (30)

**Data analysis.** Given the axion flux and cross section provided previously, we can then calculate the axion-induced event rate in the detector via (10). It is of course important to emphasise that the original purpose of the deuterium in SNO was to observe the neutral current (NC) process

$$\nu_x + d \to n + p + \nu_x,$$ (31)

which could then, in concert with measurements of the electron neutrino flux, conclusively betray the presence of solar neutrino flavour oscillations. As the final state neutrino is invisible to the detector, the signature of this process is at first sight identical to that of (9).

Of course one key difference exists in that the 5.5 MeV axions produced via (5) are monoenergetic, whilst the $^8B$ neutrinos driving (31) have a continuous energy spectrum with an endpoint near 15.8 MeV. However these spectral differences are largely washed out by the process of neutron thermalisation, which negates sensitivity to the spectral character of the input flux.

More specifically, detection of either of these phenomena rests upon the liberated neutron, once sufficiently
thermalised, being recaptured. This can occur on a
deuteron, resulting the emission of a 6.25 MeV gamma ray, or alternatively in the phase II/III SNO datasets cap-
tured onto a $^{35}$Cl nucleus, resulting the emission of 8.6 MeV in gamma rays. For the phase III dataset dedicated
neutral current detectors (NCD) were also introduced
to enable non-Cherenkov detection of NC neutrons, via
their capture onto $^3$He and the subsequent emission of a proton/triton pair carrying 0.764 MeV of energy $^{[49]}$.
Since neutron capture cross sections are suppressed by
their velocity, these processes will in general only occur
once most of the initial kinetic energy has been lost, ren-
dering SNO likely unable to distinguish between axion
and neutrino-induced dissociated events.

Whilst this apparent loss of spectral information seems
to remove the possibility of leveraging the monoenergetic
nature of the axion flux to gain greater sensitivity, it does
nonetheless simplify the required data analysis.

Following the approach employed in $^{[50]}$, we can write
the total number of dissociation events seen by SNO as

$$N^{exp} = N_a + N_d T \phi_{SSM} \int dE_{\nu} \xi(E_{\nu}) \sigma_{NC},$$

(32)

where $\phi_{SSM} = (5.87 \pm 0.44) \times 10^6$ cm$^{-2}$ s$^{-1}$ is the pred-
picted value of the $^8$B solar neutrino flux in the Standard
Solar Model, with spectral shape parametrised via

$$\xi(E_{\nu}) = 8.52 \times 10^{-6} \left(15.1 - \frac{E_{\nu}}{\text{MeV}}\right)^{2.75} \left(\frac{E_{\nu}}{\text{MeV}}\right)^2,$$

(33)

and $\sigma_{NC}$ the neutral current neutrino-deuteron interac-
tion cross section $^{[51]}$. As the resulting flux inferred by
SNO assumes that these events arise only due to NC in-
teractions,

$$\phi_{SNO} \equiv \frac{N^{exp}}{N_d T \int dE_{\nu} \xi(E_{\nu}) \sigma_{NC}},$$

(34)

and we can then write

$$\phi_{SNO} = \phi_{SSM} + \frac{\phi_d \sigma_d}{\int dE_{\nu} \xi(E_{\nu}) \sigma_{NC}},$$

(35)

where no integration over energy is required since ther-
mal broadening is negligible relative to the axion energy
at hand. The product $\phi_d \sigma_d$ is then constrained by the
combined analysis of all three phases of SNO data, which
yields $\phi_{SNO} = (5.25 \pm 0.20) \times 10^6$ cm$^{-2}$ s$^{-1}$$^{[49]}$, where
we have added errors in quadrature. Requiring that the
($\phi_{SNO} - \phi_{SSM}$) confidence interval not exceed 95 % C.L.
limits then provides the exclusion presented in Figure 1.

As can be seen, we exclude $|g^3_{aN}|$ between $2 \times 10^{-5}$
and $10^{-3}$ GeV$^{-1}$, for axion masses up to $\sim 5.5$ MeV.
For larger couplings this improves upon the $g^3_{aN}$-sensitive component of the SN1987A constraint in Ref. $^{[12]}$ arising
from additional particle-emission counts at Kamiokande,
even though this is not strictly comparable as the
SN1987A axion flux is not solely dependent on $g^3_{aN}$.

The QCD axion band bounded by the KSVZ and DFSZ
models with $\cos^2 \beta = 1$ is also shown; the latter case we exclude for axion masses between 0.3 and 13 keV, al-
though this region is in any case ruled out by astrophys-
ical considerations and direct results from PandaX-II $^{[53]}$.
Variant QCD axion models may of course differ substan-
tially from this benchmark $^{[54]}$.

Constraints on $g_{an}$ are also shown, if we assume no pre-
cise cancellation between $g_{an}$ and $g_{ap}$ then any limit on
$g^3_{aN}$ is equivalent to a limit on both $g_{an}$ and $g_{ap}$. This
assumption is not too restrictive; in the analysis of Ref. $^{[54]}$
this cancellation requires a DFSZ-type model with the
specific tuning $\tan \beta \simeq \sqrt{2}$ or $1/\sqrt{2}$.

This being the case our result can also exceed com-
parable constraints from other laboratory experiments,
and exclude regions of the parameter space for which
astrophysical constraints from SN1987A and NS cooling
are inapplicable due to axion trapping. The latter con-
straints, which in any case share some degree of degener-
acy with the SN1987A case, are not included in Figure 1 due to model-dependence and the unknown shape of the exclusion region for non-negligible axion masses.

Conclusions and discussion. The axion is a notably well-motivated aspect of physics beyond the Standard Model, and as such has been a topic of much investigation in recent years. Nonetheless, a large majority of these studies are based upon the interactions of axions with electromagnetism, leaving their couplings to nucleons and other species comparatively less well explored.

In this paper we have established a novel detection channel sensitive to precisely one of these couplings, relying upon the ability of suitably energetic axions to dissociate deuterons into their constituent neutrons and protons. In concert with the 5.5 MeV solar axion flux arising from the $p + d \rightarrow ^3\text{He} + a$ process, one can then derive a model-independent constraint on the isovector nucleon coupling $g^a_{\alpha N}$. A particularly opportune target for this search strategy is the now-completed SNO experiment, which relied upon large quantities of deuterium to resolve the solar neutrino problem.

Having derived the corresponding ‘axiodissociation’ cross section, from the full SNO dataset we exclude regions where $|g^a_{\alpha N}|$ is between $2 \times 10^{-5}$ and $10^{-3}$ GeV$^{-1}$, for axion masses up to $\sim$ 5.5 MeV, covering previously unexplored regions of the axion parameter space. This comes with the added benefit that we do not require any assumptions about the nature of dark matter, or the astrophysics of SN1987A.

If furthermore we assume no precise cancellation between $g_{\alpha N}$ and $g_{\alpha p}$, then any limit on $g_{\alpha N}^3$ is equivalent to a limit on both $g_{\alpha N}$ and $g_{\alpha p}$. In that case our result can exceed comparable constraints from other laboratory experiments, and exclude regions of the parameter space for which astrophysical constraints from SN1987A and NS cooling are inapplicable due to axion trapping. Constraints on $g_{\alpha N}/g_{\alpha p}$ from SN1987A event counts can probe equally large couplings, but at the cost of a variety of associated assumptions and uncertainties related to the modelling of SN1987A.

These findings could conceivably be improved in the future via a more sophisticated estimation of the axiodissociation cross section; we have neglected relativistic and finite-size corrections, along with D-state effects in the deuteron ground state. The existence of other axion search strategies which rely only upon nuclear couplings is also a topic of ongoing investigation.

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