The properties of van der Waals (vdW) materials often vary dramatically with the atomic stacking order between layers, but this order can be difficult to control. Trilayer graphene (TLG) stacks in either a semimetallic ABA or a semiconducting ABC configuration with a gate-tunable band gap, but the latter has only been produced by exfoliation. Here we present a chemical vapor deposition approach to TLG growth that yields greatly enhanced fraction and size of ABC domains. The key insight is that substrate curvature can stabilize ABC domains. Controllable ABC yields ~59% were achieved by tailoring substrate curvature levels. ABC fractions remained high after transfer to device substrates, as confirmed by transport measurements revealing the expected tunable ABC band gap. Substrate topography engineering provides a path to large-scale synthesis of epitaxial ABC-TLG and other vdW materials.
van der Waals (vdW) materials composed of individual atomic layers held together by vdW interactions have attracted considerable attention due to their unique physical properties that can be tuned by manipulating interlayer twisting angles\textsuperscript{1–3}, creating heterostructures\textsuperscript{4,5}, and controlling stacking configurations\textsuperscript{6–7}. One example is trilayer graphene (TLG)\textsuperscript{8}, which has two stacking configurations in its natural form. The ABA or Bernal configuration is a semi-metal with tunable band overlap\textsuperscript{9,10}, while the ABC or rhombohedral configuration is a semiconductor with a gate-tunable band gap\textsuperscript{11,12}. In fact, few-layer graphene with ABC stacking is an interesting material system. To answer this need, we develop a high-yield and characterization of ABC-TLG substrate in back-diffusion growth mode\textsuperscript{23}. Catalytic substrates epitaxies with specific properties that can be tuned by manipulating interlayer twisting angles\textsuperscript{1}. As shown schematically in Fig. 1a, TLG was synthesized on a Ni–Cu gradient alloy substrate in back-diffusion growth mode\textsuperscript{23}. Catalytic substrates were prepared by depositing a 100-nm thick Ni film on one side of a flat Cu foil. The Ni–Cu foils were then annealed at 1050 °C for 5 min to create a Ni–Cu gradient alloy substrate with a Ni-rich side and a Ni-poor side. During CVD growth, the top TLG layer forms first over the Ni-rich side of the substrate, and then the middle and bottom TLG layers grow beneath the top layer via carbon back-diffusion from the Ni-poor side\textsuperscript{23}. Additional information about the growth process is provided in the Methods section. As shown in Fig. 1b, the process resulted in high-yield TLG growth, with an areal coverage of ~30% over the entire substrate and flake sizes of 15–50 μm. All as-grown TLG domains displayed a compact hexagonal shape, attesting to their highly oriented, crystalline nature.

We performed systematic micro-ARPES and nano-ARPES measurements of the band dispersions of the material on the growth substrate, with 140 μm and 120 nm spot size respectively, to evaluate the electronic properties of the as-grown material. We directly probed the binding energy vs. momentum (\(E vs. k\_F\)) curves close to the Fermi level; these are strikingly distinctive for TLG with ABA, ABC, and AAA stacking configurations\textsuperscript{24}. The orientation, size, and distribution of graphene grains, as well as their registry with the substrate were investigated using micro-ARPES. Figure 1c shows a 3D ARPES plot, including the Fermi surface plane of the multi-graphene film, which discloses the complete electronic band structure of the graphene flakes and the metallic substrates. Strong π Dirac graphene bands are visible at the K high symmetry points of the reciprocal lattice. Moreover, well-defined \(d\) bands from Cu and/or Cu–Ni alloy are evident with binding energies of 2–4 eV. Distinctive \(d\) and \(sp\) substrate bands in the 3D ARPES plots indicate a high degree of crystallinity in the metallic substrate foils after CVD growth. The graphene-substrate registry and the orientation of the graphene flakes are revealed by the multi-graphene surface shown in Fig. 1d. A set of copper \(sp\) bands are observed dispersing in reciprocal space as expected for a copper single crystal (111) plane. Three well-defined Dirac cones are observed at \(k\_F = 1.703 \text{ Å}^{-1}\), corresponding to the π graphene bands that cross the Fermi level. In contrast to earlier reports on few-layer graphene grown by CVD\textsuperscript{24}, no arc-like shape states around the cones are observed, indicating that our graphene flakes are oriented along the TLG\textsuperscript{[110]} direction of copper, in registry with the substrate lattice\textsuperscript{25}. These results demonstrate that our process leads to epitaxial growth of TLG on the Ni–Cu gradient alloy substrate. The ARPES plot of Fig. 2a was used to select those states exclusively belonging to the graphene flakes and then record the nano-ARPES image of Fig. 2b. This image displays the intensity variations of the Dirac states at the Fermi level (yellow rectangle in Fig. 2a) throughout a large portion of the sample and reveals the distribution, size, and morphology of the graphene flakes. All the flakes exhibit identically-oriented hexagonal shapes, some more intense than the others in Fig. 2b (indicated by arrows, the intensity line scan profile of the green line is shown in Fig. 2c). To precisely and unequivocally resolve the electronic structure of each flake, the electronic band dispersion close to the Fermi level (\(E vs. momentum\)) was recorded for individual graphene grains using high energy and momentum resolution nano-ARPES\textsuperscript{26}. The most intense flakes in Fig. 2b show TLG electronic dispersion characteristics; the flake indicated by the black arrow has two bands with quadratic dispersion and one band with linear dispersion (Fig. 2f), as expected for ABA-TLG. The flake indicated by the blue arrow has a cubic band that is particularly flat at the Fermi level and two quadratic bands at similar energies that are shifted along \(k\_F\). (Fig. 2g), as expected for ABC-TLG\textsuperscript{27,28}. TLG flakes containing a mixture of both stacking types were also identified (Fig. 2h). All TLG flakes were n-doped, with the Dirac point located below the Fermi level due to the combined effects of the electrostatic surface potential and the “pillow effect” caused by surface adsorbates\textsuperscript{29–31}. These nano-ARPES results are consistent with our density-functional theory (DFT) calculations (Fig. 2i–j, Supplementary Figs. 8, 9), which qualitatively confirm the observed band dispersions for the two TLG configurations, as well as the flat substrate bands around \(-1.5 \text{ eV}\) (see Supplementary Fig. 4). Due to differences in the
density of states around the Dirac point, the induced charge transfer from the substrate to graphene leads to a greater band shift in ABA-TLG as compared with ABC-TLG, in agreement with the data in Fig. 2f–g.

Dark-field transmission electron microscopy (DFTEM) was used to probe the stacking morphology and crystallinity of the as-grown TLG. This method can provide layer number contrast for oriented graphene32 (see Methods section for details). Figure 2d shows a DFTEM image generated by selecting one of the six \{1210\} diffracted beams with the objective aperture. For oriented TLG, these diffracted beams from each layer constructively interfere, and the contrast between monolayer, bilayer, and trilayer graphene is evident in the image. The uniform appearance of the trilayer hexagon in the middle suggests that the TLG is crystalline and highly oriented. To obtain contrast between different stacking configurations, we instead selected one of the six \{0110\} diffracted beams33, which with ABC stacking completely destructively interferes and with ABA stacking only partially interferes. The \{0110\} DFTEM image (Fig. 2e) of the same region shown in Fig. 2d reveals a quasi-lamellar pattern of TLG regions with ABA and ABC stackings. Approximately 30% of the TLG flake is in the ABC configuration, twice that reported for exfoliated samples34 and larger than usual levels in graphite. We observed flakes with up to 100% ABC content (see Supplementary Fig. 2), as also observed in exfoliated samples35. AAA stacking was not observed, consistent with the ARPES results, while some twisted TLG was obtained (see Supplementary Fig. 3).

**CBSS mechanism of ABC-TLG formation.** The large-area fraction of ABC phase and the quasi-lamellar ABA/ABC domain morphology (Fig. 2e) suggest that the growth substrate properties and/or growth kinetics have an ABC-stabilizing effect. We performed ab initio calculations on flat, idealized substrates to first determine whether substrate chemistry contributes to this effect. We found that the relative energetics of multilayer graphene adsorbate/substrate systems are dominated by the interaction strength of the bottom-most graphene layer with the substrate, while differences due to variations in stacking of the upper layers are small. Energy differences computed between the most stable ABA and ABC arrangements on both Cu(111) and Ni-doped Cu(111) are therefore also small (~0.1 meV/atom) and barely within the accuracy of DFT (see Supplementary Note 1). We concluded that ABA and ABC are nearly isoenergetic on flat Cu(111) and Ni-doped Cu(111), in line with the coexistence of both structures in graphite and exfoliated TLG34. Importantly, this near equivalence between ABA and ABC energies suggests that the abundance of the two states can be tuned in finite-sized flakes by modulating other factors that slightly bias their relative energetics.

One such factor is substrate topography, which we discovered can be exploited to energetically stabilize the (typically) less prevalent ABC phase. Our growth substrates had a quasi-periodic pattern of surface corrugations (discussed further below) with typical curvatures of \(|\kappa_0| \approx 10^7 \text{m}^{-1}\) at maxima and minima (Fig. 3a). When adjacent graphene layers retain atomic registry, substrate curvature induces an in-plane interlayer strain \(\epsilon_{\text{in-plane}}(x) \approx \kappa_0 / d \approx 0.5\%\), where \(d\) is the distance between graphene layers (Fig. 3b). Graphene must stretch (compress) in regions of negative (positive) curvature to maintain registry with adjacent layers. Above a critical curvature \(\kappa_c\), interlayer slip (i.e., interlayer dislocation formation) becomes energetically preferable to maintaining atomic registry between layers at all points. For weakly bound atomic layers of the type studied here36, \(\kappa_c\) is \(\approx 10^4 \text{–} 10^5 \text{m}^{-1}\). Growth on a corrugated substrate with \(\kappa_0 > \kappa_c\) will result in arrays of interlayer dislocation lines, several types of which induce stacking shifts between ABA and ABC (i.e., domain walls = curvature-induced interlayer dislocations, see Fig. 3c and Supplementary Note 2).
To quantify these effects and identify the factors that control interlayer dislocation\textsuperscript{37} formation and domain size, we formulated a first principles-informed continuum mechanics description of the structure of vdW materials on non-flat surfaces (see Methods section for details). The dislocation character of a domain wall is denoted \( \xi = X^\xi Y \), where \( \xi \) is the domain wall line direction (\( \xi = \) zigzag or \( \xi = \) armchair), \( X \) and \( Y \) specify the stacking configuration (\( B \equiv \) Bernal/ABA, \( R \equiv \) rhombohedral/ABC) on the left and right side of the interface, respectively, and \( u \) and \( l \) specify the magnitude of \( b_0 \), the edge component of the Burgers vector \( b \) (in units of \( a/2 \), where \( a \approx 0.14 \) nm is the atomic nearest neighbor distance) between the upper two and lower two graphene layers, respectively (see Fig. 3c and Supplementary Note 2 for further details of the notation).

The results demonstrated that curvature stabilizes interlayer dislocations and that certain types of stable dislocations in turn imply the presence of ABC domains. Specifically, our model indicates that the equilibrium state changes with increasing curvature from perfect ABA to states containing interlayer dislocations (Fig. 3e). A substrate with appropriate surface curvature (red-orange region in Fig. 3e) could fully stabilize arbitrarily large ABC domains containing only \( z = R^2_2 R \) interfaces. However, the experimental values of \( k_0 \) span from ABA equilibrium (darker turquoise region) to \( z = B^4_1 B \) equilibrium (lighter turquoise region), such that some flakes may be perfect ABA, some ABC/ACB (\( z = R^2_2 R \)) or ABA/ACA (\( z = B^4_1 B \)), and some a mixture of ABA and ABC. The computed energies of the \( z = B^4_1 B \) (mixed ABA/ABC), perfect ABC, and \( z = B^4_1 B \) (ABA/ACA) states are only slightly higher than those of the equilibrium states within the region of interest, indicating that these may also be observed. This is in agreement with the identification of pure ABA, pure ABC, and flakes with both stackings via nano-ARPEES (Fig. 2f–h) and DFTEM (Fig. 2e and Supplementary Fig. 2). This stabilization of the ABC phase results from the difference in geometrically allowed partial-dislocation content between ABA and ABC stacking variants, as detailed in Supplementary Note 2 and Supplementary Figs. 10–14. Principally, ABC/ACB configurations (\( z = R^2_2 R \)) accommodate 1D curvature strain more efficiently than ABA/ACA (\( z = B^4_1 B \)) due to their larger edge character (larger \( b \), see Fig. 3d). The ABC phase is therefore preferred over an intermediate range of curvatures despite its larger bulk energy.

Our description of CBSS indicates that rich internal stacking structures will be commonplace in CVD multilayer graphene systems (Supplementary Fig. 25) and provides a framework for understanding how the interplay between corrugations and domain walls can stabilize different structures. The more prevalent views that assume internally structureless flakes (e.g.,
ABAB...-stacked multilayer graphene islands\textsuperscript{38} and/or structural domains with only simple periodic stacking sequences (e.g., a mixture of ABAB... and ABCABC...\textsuperscript{33}) are not likely representative of actual states.

To directly test the CBSS mechanism, we marked a CVD-grown sample such that DFTEM images of domain wall morphologies could be mapped back to AFM images of the substrate topography at the precise location where growth occurred (see Supplementary Note 3 and Supplementary Fig. 19 for experimental details). Figure 3f shows that the dominant domain wall direction is precisely aligned with that of the substrate corrugations, and further that individual domain walls are strongly correlated with lines of maximum curvature (indicated by white arrows in Fig. 3f). Imperfect correlation is expected due to substrate corrugation irregularities and changes in domain wall configuration induced during cooling and transfer. Importantly, we found that substrate regions with lower than average corrugation curvatures (e.g., at grains with atypical surface crystal orientations) yielded significantly less ABC coverage than those with curvatures in or near the ABC/ACB-stabilizing range shown in Fig. 3c. This is seen clearly in the IR-SNOM stacking map (Supplementary Fig. 6) for a single TLG flake that spans three different Cu grains. The map shows 40% ABC coverage over one grain that has near-optimal curvature ($\sim -1.2 \times 10^7$ m\(^{-1}\)) and only 7% ABC coverage over the other two grains which have significantly lower curvatures ($\sim -1.2 \times 10^6$ m\(^{-1}\)). Further details of the IR-SNOM technique are provided below.

Previous studies have shown that ABC-TLG domain size can be manipulated using an electric field\textsuperscript{39} or mechanical force\textsuperscript{40} to drive domain wall motion. Here we have uncovered a new factor, substrate curvature, that governs ABC-TLG domain size and shape.
during synthesis. Substrate corrugations of the type seen here, long observed on graphene growth substrates but poorly understood, have recently been shown to form and coarsen beneath graphene during growth.\(^\text{[41]}\) We propose (and provide evidence) that the primary driving force for this phenomenon is the reduction of the total step/curvature-induced interlayer disorder/dislocation energy \((E_{\text{disreg}} + E_{\text{disloc}}, \text{see Methods section})\) as substrate step edges merge into increasingly coarse corrugations (see Supplementary Note 5 and Supplementary Fig. 22). The resulting corrugation evolution during growth feeds back into graphene stacking domain morphology in a co-evolving process. Incorporating this overlayer-driven corrugation kinetics into our continuum model, we obtain a time-dependent description of domain wall energetics during simultaneous corrugation coarsening and graphene growth (see Supplementary Note 5 and Fig. 3e).

These insights indicate that ABC yield can be controlled and optimized by engineering curvature through tailoring synthesis parameters (growth time, temperature, substrate chemistry, crystallography). Accordingly, increasing growth time from 1 to 6 h led to a monotonic increase in the final average peak corrugation curvatures (measured on our Cu (111) substrates) from \(-7.0 \times 10^6\) to \(-1.4 \times 10^7\) \text{m}^{-1} (Fig. 3g and Supplementary Fig. 23). ABC yield also increased monotonically from \(-22\%\) to \(-39\%\) between 1 and 3 h, before decreasing to \(-36\%\) at 6 h (Fig. 3g and Supplementary Fig. 24). The increase in ABC yield to a maximum at substrate curvatures \(-1.0\) to \(-1.2 \times 10^7\) \text{m}^{-1} is in good agreement with the predictions of Fig. 3e, and the decrease at 6 h is consistent with our expectation of a finite range of optimal curvatures. These results substantiate our physical description of CBSS and demonstrate that the growth process can be designed to control and optimize ABC yield. More precise control and higher yields may be achievable with further exploration of the effects of growth temperature, substrate chemistry, and substrate crystallography (see Supplementary Note 5).

We performed additional experiments to confirm that curvature-stabilized ABC domains were preserved and exhibited appropriate electronic properties after transfer and conformation to flat dielectric substrates commonly used for device fabrication. TLG flakes were transferred to a SiO\(_2\) substrate and imaged with infrared scanning near-field optical microscopy (IR-SNOM; Fig. 4a). In this measurement, infrared light (red beam in the figure) is focused onto a metal-coated AFM tip, and the backscattered light is collected by a detector in the far field. Local infrared conductivities are thus obtained across the TLG flake, generating contrast between ABA (green) and ABC (purple) regions.\(^\text{[42]}\) IR-SNOM is uniquely suited for the task of analyzing the domain structure of the TLG synthesized here because its tip-enhanced signal offers \(-20\) nm spatial resolution (diameter of the metallic AFM tip), greatly superior to the \(-1\) \text{nm} typically achieved by Raman spectroscopy.\(^\text{[34]}\)

Figures 4b, d show TLG flake topographies as measured by AFM. The flake height is uniform across the hexagonal domains, except at the \(-3\) to \(-7\) \text{nm} high wrinkles visible as white lines. The corresponding IR-SNOM image, however, exhibits distinct contrast between ABA and ABC regions (Fig. 4c, e). Both ABA-TLG and ABC-TLG were observed via IR-SNOM after transfer to SiO\(_2\), and three striking phenomena were identified:

1. Quasi-lamellar stacking domains, similar to the DFTEM image of Fig. 2e, were observed. (2) ABA and ABC regions identified by IR-SNOM were \(-10\) to \(-2\) \text{nm} wide (\(-1\) \text{nm}) on average than those seen by DFTEM, with significantly reduced domain wall density (compare Fig. 2e with Fig. 4c, e). (3) Wrinkles and ABA–ABC domain walls were highly correlated (see green arrows in Fig. 4b, c). TLG flakes with armchair (zigzag) domain wall line directions exhibited an average ABC coverage of \(-28\%\) (59\%) and an average area of \(1.4 \text{µm}^2\) (5.6 \text{µm}^2) (see Supplementary Fig. 7).

These phenomena can be understood in light of the physical picture described by our continuum model. First, the difference in ABC-TLG yield between samples with zigzag and armchair domain walls is consistent with the prediction of our continuum model that maximum ABC stabilization occurs at the zigzag direction (see Fig. 3e and Supplementary Fig. 10). Second, the growth substrate possesses a quasi-periodic array of peaks and valleys with nearly equal but opposite curvature (Fig. 3a), which favors the creation of TLG with a quasi-periodic array of domain walls with alternating sign. After removal of the domain wall-stabilizing Ni–Cu substrate and transfer to flat SiO\(_2\), many adjacent interlayer dislocation pairs will be attracted toward each other, and those pairs whose Burgers vectors sum to zero will fully annihilate upon contact, as described in Supplementary Figs. 15–18. The average ABA and ABC domain sizes are therefore expected to increase upon transfer to flat SiO\(_2\). Strikingly, we found that large-area CVD ABC-TLG can be reliably retained after transfer onto an hBN substrate (Supplementary Fig. 26). This stands in sharp contrast to the case for exfoliated graphene, where it is reported that ABC-TLG is almost always converted to ABA-TLG after transfer onto hBN. Our CVD approach is therefore expected to have a significant impact on research directed at the Mott-insulator state\(^\text{[43]}\) and tunable superconductivity\(^\text{[44]}\) in TLG.

**Transport measurement of ABC-TLG.** The large ABC-TLG and ABA-TLG domain sizes on SiO\(_2\) as identified by IR-SNOM allowed us to fabricate FET devices and perform transport measurements on TLG regions with different stacking configurations. Confirmation of their expected electronic behavior is critical for potential applications. As illustrated in the inset of Fig. 4f, FET devices were created in dual-gate configurations using 40 nm thick Al\(_2\)O\(_3\) dielectric layers deposited by atomic layer deposition as the top-gate dielectric and 250 nm thick thermally grown SiO\(_2\) as the bottom-gate dielectric. We measured the resistance of TLG channels as a function of the top and bottom-gate voltages at a temperature of 1.8 K. Figure 4f shows resistance vs. top-gate voltage (\(R-V_{\text{TG}}\)) curves of an ABC-TLG channel. The existence of a tunable band gap in the material is evidenced by the increase in the on/off ratio as the strength of the out-of-plane electric field is increased. The same measurement showed that a sizeable ABC band gap was also achieved at room temperature (Supplementary Note 4 and Supplementary Fig. 21), further evidence of the high quality of our epitaxially-grown TLG. At 1.8 K, an on/off ratio of more than 3000 was observed, comparable to exfoliated samples.\(^\text{[35,46]}\) No such increase was observed for the ABA FET (Fig. 4g), in good agreement with its predicted band structure and measurements by others on exfoliated samples.\(^\text{[7,45]}\)

**Discussion**

We have demonstrated a scalable and controllable approach to CVD growth of TLG with an enhanced yield of large ABC-stacked domains. The growth strategy was based on a Ni–Cu gradient alloy substrate that facilitates the back-diffusion growth mode. The key mechanism introduced and underlying the approach is curvature-based stacking selection (CBSS); the use of substrate curvature on the nanoscale to generate interlayer dislocations and locally stabilize ABC domains. The quasi-periodic corrugated topography of our growth substrate (commonly observed) typically generates alternating lamellar regions of ABC and ABA, as revealed by DFTEM and IR-SNOM measurements. An optimal range of curvatures, tunable through growth time, leads to maximized ABC yield, consistent with our continuum CBSS model predictions. The coarsening of substrate topography...
to 100 V (20 V steps). The net doping (n-type or p-type) varied from device to device depending on details of the fabrication process in which charged impurities are introduced.

**Methods**

**TLG synthesis and transfer.** The TLG growth was carried out in an atmospheric pressure CVD system with a 1-inch furnace (Lindberg Blue M, Thermo Scientific Co.). Cu foils of 25 µm thickness (Item #46365, Alfa Aesar) were cleaned with 5.4% HNO3 for 40 s and two DI water baths for 2 min each. A nickel film of 100 nm thickness was sputtered onto one side of the Cu foil (Lesker PVD75 DC/RF Sputter System). Ni–Cu foils were cut into 1 cm × 4 cm pieces and then loaded into the CVD furnace. The furnace was ramped to 1050 °C at a rate of 60 °C/min in a flow of 300 sccm Ar. TLG was grown using 1.8 sccm CH4 (1% in Ar) + 30 sccm H2. The reactor was then rapidly cooled to room temperature in a flow of 10 sccm H2 and 1000 sccm Ar.

PMMA (MicroChem Corp., PMMA950, A4) was spun over the surface of the TLG as grown on Ni–Cu foils and then baked at 100 °C for 2 min. The substrate was removed by an etcher solution (Transene Company, Inc. CE-100). The PMMA supported TLG was cleaned in 10% HCl solution and two water baths, and was transferred onto a 250 nm SiO2/Si substrate with prefabricated gold makers. After air drying and baking at 150 °C for 3 min, PMMA was removed by soaking the sample in acetone overnight and cleaning with IPA. TLG on SiO2/Si substrates were annealed in H2/Ar forming gas at 400 °C for 1 h before IR-SNOM characterization.

**IR-SNOM.** Scattering-type scanning near-field optical microscopy is based on tapping mode atomic force microscopy (AFM). A metallic AFM tip is illuminated with a focused CO2 laser beam with wavelength 10.6 µm and the enhanced local field under the tip interacts strongly with the sample underneath it. The elastically

Fig. 4 IR-SNOM and electron transport characterization of ABC-TLG and ABA-TLG. a Schematic of IR-SNOM for characterization of ABC-TLG on a SiO2 substrate. b, d AFM topography image of TLG flakes showing uniform heights across the entire flake except along wrinkles (white lines). The height scale is 2 nm. c, e Corresponding IR-SNOM image of the TLG flake in b and d. ABA-TLG and ABC-TLG show different infrared contrasts, which are absent in the topography image. f has primarily armchair domain walls, and e has primarily zigzag domain walls. (contrast scale: 1.43 V in c and 2.20 V in e). Green arrows in c indicate correlated wrinkles and ABA-ABC domain walls. f R–V TG characteristics of CVD ABC-TLG at 1.8 K. Each curve was measured with a fixed VBG ranging from –120 V to 100 V (20 V steps). The on/off ratio increases with VBG due to the band gap opening of ABC-TLG. The inset shows a schematic of the dual-gated TLG device. g R–V TG characteristics of CVD ABC-TLG at 1.8 K. Each curve was measured with a fixed VBG ranging from –80 V to 100 V (20 V steps). The net doping (n-type or p-type) varied from device to device72, depending on details of the fabrication process in which charged impurities are introduced.
scattered light containing the local optical properties of the sample substrate is collected by a MCT (HgCdTe) detector in the far field. Near-field optical images with spatial resolution of sub 20 nm can be achieved simultaneously with topography by recording the scattered light while scanning the sample. ABA/ABC graphene have different optical properties at 10.6 μm due to their different band structures and thus can be differentiated in the near-field images. In bilayer graphene, the contrast of domain walls in near-field images stems from surface plasmon re-scattering from the domain walls and feature a single or double bright line depending on the domain wall type47. Operation in tapping mode rather than contact mode40 prevents imaging-induced domain wall motion, and no such motion was observed in these experiments.

AFM. An atomic force microscope (AFM, Icon Bruker) equipped with a probe with a tip radius of 10 nm (HQ-300-Au, Oxford Instruments) was used to characterize the topography of the growth substrate, in a different facility from that in which IR-STM measurements were performed.

Fabrication of dual-gate TLG FET structures. ABA-TLG and ABC-TLG regions were first identified by IR-STM. ABA- and ABC-TLG channels were then defined by e-beam lithography and oxygen plasma etching (Pressure: 1.23 Torr, Power: 50 W, Duration: 35 s). The remaining e-beam resist (PMMA950 CA, MicroChem Corp.) was removed using acetone and isopropanol (IPA). The top contact metallization for the FET device (5 nm Cr/40 nm Au) was deposited by e-beam lithography followed by thermal evaporation. After liftoff process, the device was annealed at 225 °C in the forming gas of 1000 sccm Ar + 250 sccm H2 for 1 h to reduce the PMMA residuals on TLG channels. The devices were spin-coated with a HSQ buffer layer (1% in MBK, 6000 rpm for 60 s, softbake at 80 °C for 4 min), followed by atomic layer deposition (Cambridge Nanotech S200) of 40 nm Al2O3 as the top-gate dielectric. Lastly, e-beam lithography was carried out to deposit 5 nm Ti/40 nm Au top-gates on the Al2O3 dielectric to form the dual-gate FET devices.

Electrical transport measurement. Low temperature electrical transport measurements were performed in a Quantum Design Physical Property Measurement System at an ambient He pressure of ~5 Torr. Transport measurements were recorded using the drain as a common ground for the source and gates. Voltages for top and back gates were independently controlled by Keithley 2410 and 2400 sources, respectively. Source-drain current-voltage data with mV scale source bias was used to determine the channel resistance for each gate configuration. Source-drain current-voltage data with mV scale source bias was used to determine the channel resistance for each gate configuration. The total dislocation line energy (per unit length) is

\[ E_{\text{disloc}} = \frac{3}{2} \sum_{i=1}^{n} L_{\text{Cu}} N_{\text{i}} \left( \frac{\nu_i}{\alpha} \left( E_{\text{edge}} \sin^2 \theta + E_{\text{core}} \cos^2 \theta \right) + \frac{2\kappa_i}{L_{\text{Cu}}} \left( \frac{E_0}{4} + \frac{B}{2} \right) \right) \]

where \( \nu_i = d_i N_i - \varepsilon_{\text{disloc}} \) is the elastic strain and \( \varepsilon_{\text{disloc}} (x) = d_i(x)/|x| (x) + \sum_{j \neq i} d_j(x) \) is the geometric strain.

DFTEM. TLG was transferred onto a Cu grid with an amorphous carbon support. TLG was transferred onto a Cu grid with an amorphous carbon support. The 002 diffraction spot with the objective aperture gives layer number contrast for layers (as illustrated in Fig. 3b), and elastic strain \( \varepsilon_{\text{el}} \) is that introduced by curvature under the condition of epitaxial registry between layers (as illustrated in Fig. 3b), and elastic strain \( \varepsilon_{\text{el}} \) is that introduced by interlayer dislocations. The bulk energy of the trilayer is \( E = E_{\text{core}} + E_{\text{inter}} + E_{\text{disloc}} \)

Continuum model for CBSS in vdW materials. The total energy of an elastic multilayer system (weakly bonded sheets) was divided into contributions from in-plane disregistry strain, layer intercalation, and stacking phase bulk energies; \( E_{\text{disloc}} = E_{\text{edge}} + E_{\text{core}} + E_{\text{disloc}} \). For trilayer graphene on corrugated Cu (111), the substrate topography was assumed to vary only along \( x \) such that the disorder energy over a region of size \( L_{\text{Cu}} \) (per unit length) is

\[ E_{\text{disloc}} = \sum_{i=1}^{n} L_{\text{Cu}} N_{\text{i}} \left[ \frac{\nu_i}{\alpha} \left( E_{\text{edge}} \sin^2 \theta + E_{\text{core}} \cos^2 \theta \right) + \frac{2\kappa_i}{L_{\text{Cu}}} \left( \frac{E_0}{4} + \frac{B}{2} \right) \right] \]

where \( \nu_i = d_i N_i - \varepsilon_{\text{disloc}} \) is the elastic strain and \( \varepsilon_{\text{disloc}} (x) = d_i(x)/|x| (x) + \sum_{j \neq i} d_j(x) \) is the geometric strain. \( E_{\text{edge}} = 340 \text{ N/m}^{3/2} \) is the 2D Young’s modulus of graphene, \( x \) is the interlayer index (\( i = 1, 2, 3 \)) correspond to C1-C2, C2-C3, and C3-C1, respectively; see Fig. 3b); \( E_{\text{disloc}} \) is the dislocation Burgers vector magnitude along \( x \) (edge component), \( N_i \) is the integer dislocation density between \( x = 0 \) and \( x = L_{\text{Cu}} \). The in-plane misfit strain flat between flat layers in \( d_i = 0.335 \text{ nm} \) is the interlayer separation. We separate geometric strains from elastic strains in \( E_{\text{disloc}} \) to emphasize the physical competition between these two effects. Geometric strain \( \varepsilon_{\text{el}} \) is that introduced via curvature under the condition of epitaxial registry between layers (as illustrated in Fig. 3b), and elastic strain \( \varepsilon_{\text{el}} \) is that introduced by interlayer dislocations. Without dislocations, the entire geometric strain is stored as elastic energy within the system. With a particular amount of dislocations, the introduced elastic strain exactly offsets the geometric strain, and the strain energy goes to zero. With this form of \( E_{\text{disloc}} \), the strain reference state is that in which a given graphene layer rests strain-free on either the substrate (\( i = 3 \)) or the graphene layer below it (\( i = 1 \) or 2). This form also invokes the assumption that dislocations relieve strain uniformly across each local peak or valley. The total dislocation line energy (per unit length \( y \) adapted from ref. 37) was expressed as
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**Author contributions**

A.T.C.J. and F.W. directed the project. Z.G. conceived and performed the TLG growth experiments. S.W. and F.W. performed IR-SNOM measurements. J.B. developed the continuum model under the supervision of D.J.S. J.G. performed DFT calculations under the supervision of A.M.R. W.P., Q.Z. and Z.G. performed TEM characterizations under the supervision of M.D. FET devices were fabricated made by Z.G. and Q.Z. under the supervision of A.T.C.J. and Z.L. J.M.K. and S.H.P. performed electrical measurements. J.A., H.Y., C.C., and M.C.A. performed ARPES and nano-ARPES experiments. Z.G., J.B., J.G. and A.T.C.J. wrote the paper with input and approval from all authors.

**Competing interests**

The authors declare no competing interests.

**Additional information**

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