Formation of Interstellar Silicate Dust via Nanocluster Aggregation: Insights From Quantum Chemistry Simulations

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The issue of formation of dust grains in the interstellar medium is still a matter of debate. One of the most developed proposals suggests that atomic and heteromolecular seeds bind together to initiate a nucleation process leading to the formation of nanostructures resembling very small grain components. In the case of silicates, nucleated systems can result in molecular nanoclusters with diameters \( \leq 2 \) nm. A reasonable path to further increase the size of these proto-silicate nanoclusters is by mutual aggregation. The present work deals with modeling this proto-silicate nanocluster aggregation process by means of quantum chemical density functional theory calculations. We simulate nanocluster aggregation by progressively reducing the size of a periodic array of initially well-separated nanoclusters. The resulting aggregation leads to a set of silicate bulk structures with gradually increasing density which we analyze with respect to structure, energetics and spectroscopic properties. Our results indicate that aggregation is a highly energetically favorable process, in which the infrared spectra of the finally formed amorphous silicates match well with astronomical observations.

Keywords: interstellar medium, silicate grains, periodic DFT simulations, infrared spectra, nanocluster aggregation

INTRODUCTION

Interstellar matter consists of gaseous molecules and submicron solid state particles commonly referred to as dust grains. Ninety nine percentage of the interstellar mass belongs to the former group while a meager 1% to the latter one. This matter is not evenly distributed and often accumulates in condensed regions between stars, forming interstellar clouds (Tielens, 2013; van Dishoeck, 2014). Despite making up only a tiny fraction of the interstellar mass, dust grains are pivotal constituents which assist in the build-up the molecular diversity and complexity of the interstellar medium (ISM) (Williams and Herbst, 2002; Hama and Watanabe, 2013). Indeed, the formation of different simple molecules [some of them of fundamental relevance such as H₂, (Kerkeni and Bromley, 2013; Vidali, 2013; Navarro-Ruiz et al., 2014a, 2015, 2016) H₂O (van Dishoeck et al., 2013; Molpeceres et al., 2019) and CH₃OH (Watanabe et al., 2003; Rimola et al., 2014)] as well as complex organic molecules (Öberg, 2016; Herbst, 2017; Zamirri et al., 2019b) (e.g., CH₃CHO or NH₂CHO) (Enrique-Romero et al., 2016, 2019; Rimola et al., 2018) has been postulated to exclusively occur on the surface of grains. Co-adsorption at catalytic surface sites accelerate these formation reactions, which would not otherwise occur in the gas phase.
In the ISM, dust particles can be found as bare grains of refractory materials or covered in ices, depending on the conditions of the interstellar clouds where they are found. In diffuse clouds the temperature is typically between 50–100 K with gas densities in the range $10^{-2} \text{ cm}^{-3}$. Here, bare grains predominate because UV photons can penetrate the cloud, destroying any molecular complex species. Grains consist of either carbonaceous materials (Ehrenfreund and Charnley, 2000; Tielens, 2008) or silicates (Henning, 2010) (i.e., refractory materials), depending on the C/O ratio where they nucleate, grow and form. In dense molecular clouds (with temperatures as low as $5–10$ K and a gas density of $\sim 10^5 \text{ cm}^{-3}$), the low permeability of UV photons into the cloud allows the formation/accretion of simple volatile species, which convert into ice mantles covering the refractory grains. The most predominant component of the interstellar ices is H$_2$O, but other species are also relatively abundant, such as NH$_3$, CO, CO$_2$, and CH$_3$OH (Boogert et al., 2015).

Most bare interstellar grains are made of silicates, which are a class of naturally occurring inorganic materials with a large diversity in chemical composition and structural properties. All silicates are based on the [SiO] building block with divalent cations compensating the negative charge. In interstellar grains the most common cation is Mg$^{2+}$, followed to a lesser extent by Fe$^{2+}$, as dictated by the relative interstellar abundances. Two main classes of interstellar silicates have been identified: olivines and pyroxenes, with general chemical compositions Mg$_{x}$Fe$_{2-x}$SiO$_4$ and Mg$_x$Fe$_{1-x}$SiO$_3$ (x = 0–1), respectively. These interstellar grain silicates are usually structurally amorphous, although crystalline silicates have also been detected (Molster and Kemper, 2005). Evidence of amorphyicity is provided by astronomical infrared (IR) observations, where mid-IR measurements show two broad bands centered at $9.7 \mu \text{m}$ ($\sim 1,100 \text{ cm}^{-1}$) and $18 \mu \text{m}$ ($\sim 550 \text{ cm}^{-1}$) (Henning, 2010), attributed to the $\nu$(SiO) stretching and $\delta$(OSiO) bending modes. These bands are usually found to be heavily broadened, which is indicative of the wide distribution of bond lengths and angles characteristic of amorphous systems. We note that this assignment of broadened bands to amorphous silicate grain should be used with care in the case of very small grains (Zamirri et al., 2019a).

The elementary steps leading to silicate grain formation is not yet fully understood. The commonly held current view is that silicate dust nucleates in outflows of dying stars, in which atomic and molecular seeds bind together to initiate the nucleation process (Weinberger, 2005; Ercolano et al., 2007; Jones, 2007; Matsuura et al., 2011). Some thermodynamically viable pathways for the initial stages of silicate nucleation in circumstellar environments have been studied by computational chemistry techniques, indicating that heteromolecular aggregation of Mg, SiO and H$_2$O could be a plausible mechanism, rather than direct nucleation of atomic O, Mg and Si (Goumans and Bromley, 2012, 2013). The silicate dust grains formed in such processes are thought to be of the order $0.1 \mu \text{m}$ in diameter (dust grain monomers) when they leave the star and enter the ISM. There, these grains are subject to supernovae shockwaves and dust grain collisions which shatter these grains into small nanosized fragments (Jones et al., 1996; Hirashita and KOBayashi, 2013). There is also laboratory evidence that small silicate dust grains may (re)form in the ISM (Roullé et al., 2014). It is thus estimated that the ISM could contain a significant population of nano-sized silicates (Li and Draine, 2001b), which will eventually form part of the diffuse and dense clouds.

Interestingly, proto-silicate nanoclusters have properties that match relatively well with the physico-chemical features of very small grain (VSG) components (of size $\leq 20 \text{ nm}$) (Li and Draine, 2001a; Roullé et al., 2014), the optical properties of which cannot be described by bulk material measurements. VSGs may be responsible for the UV bump in the IS extinction curve and a significant fraction of the mid-IR emission (Rapacioli et al., 2005; Pilleri et al., 2012, 2015). Although carbonaceous materials (e.g., polycyclic aromatic hydrocarbons, hydrogenated amorphous carbon) have been advocated to be the main constituent of VSGs, there could also be a significant component formed from proto-silicate nanoclusters/nanoparticles. VSGS can be understood as intermediate species from which larger silicates (i.e., grain monomers) are formed from the nucleation seed. A reasonable process would involve the production of different proto-silicate nanoclusters driven by harsh external phenomena (e.g., cosmic ray hits or shock waves) and subsequent aggregation by intermolecular attractive forces between nanoclusters. Interestingly, since nanoclusters are inherently not crystalline-like (Escatllar et al., 2019; Zamirri et al., 2019a), direct aggregates are expected to exhibit an amorphous structural state.

Quantum chemical computations have been used to investigate on the physico-chemical properties of interstellar silicates (Goumans and Bromley, 2011; Kerkeni and Bromley, 2013; Navarro-Ruiz et al., 2014a,b; Navarro-Ruiz et al., 2015, 2016; Oueslati et al., 2015; Kerkeni et al., 2017, 2019; Molpeceres et al., 2019), demonstrating the extreme usefulness of this approach by providing unique results at an atomic scale related to their structure, reactivity and vibrational features. In the present work, the aggregation between proto-silicate nanoclusters to form silicate bulk aggregates is investigated by means of quantum chemical simulations. To this end, a modeling strategy based on the gradual reduction in size of a periodic unit cell centered on a proto-silicate nanocluster, thus decreasing the distance between repeated nanoclusters, is employed. The resulting increasingly condensed systems during this procedure have been analyzed from a structural, energetic and spectroscopic points of view giving new insights into the plausibility of the proto-silicate aggregation processes.

**METHODS**

Theoretical calculations were carried out with the CRYSTAL14 code (Dovesi et al., 2014); a program dedicated to simulating all-electron periodic and molecular systems. Simulations were performed with density functional theory (DFT) calculations using the hybrid B3LYP functional (Lee et al., 1988; Becke, 1993) in combination with the following Gaussian basis sets: (8s)-(511sp)-(1d) for Mg, (8s)-(631sp)-(1d) for Si,
and (8s)-(411sp)-(1d) for O. A reliable performance of this methodology for simulating the structure and spectroscopic properties of silicates is evidenced by different theoretical works, where results of DFT calculations using the B3LYP functional are found to compare very well with experimental measurements related to IR, Raman and reflectance spectroscopy (Noel et al., 2006; De La Pierre et al., 2011, 2013; Navarro-Ruiz et al., 2014b; Martínez-González et al., 2018).

The shrinking factor of the reciprocal space net was set to 3, defining a total of 14 k points in the irreducible Brillouin zone (IBZ) (Monkhorst and Pack, 1976). The overlap integrals controlling the Coulomb and exchange series were set to $10^{-6}$ and $10^{-16}$. The SCF criterion was set to $10^{-7}$ Hartrees. Geometry optimizations were performed using the quasi-Newton algorithm, combining the quadratic step (BFGS scheme) with a linear one (Civalleri et al., 2001; Doll, 2001).

Simulated IR spectra were obtained by computing the vibrational frequencies of the studied systems at the $\Gamma$ point (point $k = 0$ in IBZ) within the harmonic approximation. The Hessian matrix was obtained numerically (i.e., via the central difference formula), in which second-energy derivatives are calculated by displacing each of the $3N$ optimized nuclear positions by a small amount ($u = 0.003$ Å) (Pascale et al., 2004). The SCF criterion convergence to numerically construct the Hessian matrix was set to $10^{-11}$ Hartrees in order to ensure sufficiently accurate numerical derivatives for calculating frequencies. IR intensity values of the normal modes were calculated through the variation of the dipole moment along the corresponding modes using a set of localized Wannier functions (Zicovich-Wilson et al., 2001, 2002). We note that anharmonicity is very unlikely to be significant in our systems as they do not contain light atoms (e.g., H) and the aggregation process is interpreted to occur at the very low temperatures of the ISM, and thus only low energy vibrational states are populated. Accordingly, we consider the harmonic approximation to be sufficiently accurate for the description of the vibrational spectra.

Visualization and manipulation of the structures, including visual inspection of the calculated frequencies for band assignment, have been carried out with the MOLDRAW program (Ugliengo et al., 1993). Figures were rendered with the POVRAY program.

## RESULTS AND DISCUSSION

The underlying idea is to assess if aggregation of proto-silicate nanoclusters can result in the formation of silicate grains present in the ISM. To this end, construction of bulk silicate structures from gradually bringing together molecular silicate nanoclusters was firstly performed. Then, a structural and energetic analysis of the obtained structures was carried out to assess the stability of these aggregates with respect to the respective bulk crystalline silicate system. Finally, simulated IR spectra were compared with observational data for actual IR silicates in the ISM. Cartesian/fractional coordinates of the studied systems are available in the Supplementary Material.

### Construction of Aggregated Silicates

The initial structure from which the aggregated silicate systems are generated is the Mg$_6$Si$_3$O$_{12}$ nanocluster (Sil-0 in Figures 1, 2), which has the forsterite stoichiometry (i.e., Mg$_2$SiO$_4$) and contains three formula units. Sil-0 was found as one of the most energetically stable nanocluster isomers of this size in global optimization searches using Monte Carlo basin hopping approach (Escatllar et al., 2019). In Escatllar et al. (2019) DFT based calculations were carried out using the PBE0 hybrid functional, while our work employed the B3LYP hybrid functional. Despite this methodological difference, structural parameters for Sil-0 provided by both methods compare extremely well.

Our “virtual” aggregation process (represented in Figures 1, 2) is explained as follows. The first step was to apply periodic boundary conditions to Sil-0. That is, the nanocluster was introduced inside a cubic box (i.e., the unit cell) that was repeated periodically in the three spatial dimensions. The initial lattice parameters of the unit cell were set to $a = b = c = 12$ Å and
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Once this situation was reached (i.e., interaction between replicated nanoclusters), during this aggregation phase both internal atomic positions and lattice cell parameters were optimised in order to better allow the interacting nanoclusters to reach a stable relaxed energy minimum. This final aggregation process led to the formation of several extended amorphous silicates with different structures and densities (see Sil-1_4, Sil-1_5, and Sil-1_6 and Table 1).

Finally, we note that the structures of the resulting amorphous silicates derived from our aggregation procedure depend on the initial orientation of the nanocluster inside the periodic box. This effect is shown in the aggregated structures in Figures 1 and 2, respectively, where in the latter case, the nanocluster was rotated 45° with respect to the c axis as compared to the former. This change in initial conditions was found to significantly influence the detailed atomic structures during aggregation, especially those generated in the final aggregation steps, in which the unit cell parameters were optimized (e.g., compare Sil-1_4, Sil-1_5 and Sil-1_6 with Sil-2_4, Sil-2_5, and Sil-2_6, respectively).

Structural and Energetic Analysis

Figures 1, 2 show the optimized silicate systems adopting the abovementioned nanocluster aggregation procedure. The first generated structures (Sil-1_1/Sil-2_1 and Sil-1_2/Sil-2_2 in Figures 1, 2) are periodic arrays of isolated silicate nanoclusters. Since these structures do not significantly interact with respective

 TABLE 1 | Densities (in g cm\(^{-3}\)) and lattice cell parameters (distances in Å and angles in degrees) of the periodic silicate structures shown in Figures 1, 2.

| Figure 1   | Density | a    | b    | c    | α    | β    | γ     |
|------------|---------|------|------|------|------|------|-------|
| Sil-1_1    | 0.403   | 12.0 | 12.0 | 12.0 | 90.0 | 90.0 | 90.0  |
| Sil-1_2    | 0.697   | 10.0 | 10.0 | 10.0 | 90.0 | 90.0 | 90.0  |
| Sil-1_3    | 0.956   | 9.0  | 9.0  | 9.0  | 90.0 | 90.0 | 90.0  |
| Sil-1_4    | 1.687   | 7.804| 7.918| 6.809| 83.3 | 94.1 | 82.9  |
| Sil-1_5    | 2.451   | 7.821| 7.544| 5.643| 111.7| 111.8| 75.0  |
| Sil-1_6    | 2.940   | 7.5  | 6.1  | 5.8  | 101.1| 72.3 | 77.4  |
| Sil-1_4c   | 1.361   | 8.0  | 8.0  | 8.0  | 90.0 | 90.0 | 90.0  |
| Sil-1_6c   | 2.032   | 7.0  | 7.0  | 7.0  | 90.0 | 90.0 | 90.0  |

| Figure 2   | Density | a    | b    | c    | α    | β    | γ     |
|------------|---------|------|------|------|------|------|-------|
| Sil-2_1    | 0.403   | 12.0 | 12.0 | 12.0 | 90.0 | 90.0 | 90.0  |
| Sil-2_2    | 0.697   | 10.0 | 10.0 | 10.0 | 90.0 | 90.0 | 90.0  |
| Sil-2_3    | 0.956   | 9.0  | 9.0  | 9.0  | 90.0 | 90.0 | 90.0  |
| Sil-2_4    | 1.994   | 8.228| 5.746| 7.770| 95.5 | 88.4 | 73.2  |
| Sil-2_5    | 2.914   | 5.143| 7.729| 6.489| 87.6 | 96.9 | 69.7  |
| Sil-2_6    | 2.988   | 5.822| 7.573| 6.319| 93.8 | 116.0| 69.5  |
| Sil-2_4c   | 1.361   | 8.0  | 8.0  | 8.0  | 90.0 | 90.0 | 90.0  |
| Sil-2_5c   | 2.032   | 7.0  | 7.0  | 7.0  | 90.0 | 90.0 | 90.0  |
| Sil-2_6c   | 2.371   | 6.0  | 7.0  | 7.0  | 90.0 | 90.0 | 90.0  |
| forsterite | 3.150   | 4.789| 10.254| 6.009| 90.0 | 90.0 | 90.0  |

\(α = β = γ = 90^\circ\). Once the periodic system was generated, the atomic positions of the nanocluster were optimized, keeping the lattice parameters fixed to avoid interactions between replicated nanoclusters. Due to the relatively large values of a, b and c, the first system is simply a relatively isolated Sil-0 nanocluster inside the unit cell, which keeps its molecular structure (see Sil-1_1 in Figure 1), meaning that there are no significant interactions between periodically replicated nanoclusters.

From this starting point, the values of a, b and c were progressively decreased (shown in Figure 1), hence reducing the size of the unit cell, in which the internal atomic positions of the system were relaxed with fixed lattice parameters. With each reduction in cell size, the replicated nanoclusters were closer to each other (see Sil-1_1 and Sil-1_2 structures of Figure 1), up to a point in which interaction between nanoclusters took place. Indeed, structure Sil-1_3 of Figure 1 shows the formation of Mg-O bonds between two adjacent nanoclusters. At this point, we can consider that aggregation is starting to occur.

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images (the closest inter-cluster distances are ≈6.1 Å and ≈4.0 Å, respectively), they do not suffer structural variation with respect to the original nanocluster.

The first replica-interacting systems (structures Sil-1_3 and Sil-2_3 in Figures 1, 2) show the formation of Mg-O bonds between images forming a square (MgO)$_2$ ring. These interactions take place when the unit cell parameters are $a = b = c = 9$ Å. This suggests that inter-cluster Mg-O interactions could trigger the silicate aggregation between nanoclusters. This is reasonable since interaction between these two atom types is essentially electrostatic (i.e., formally between Mg$^{2+}$ and O$^{2-}$ ions). From these initially interacting structures, slight reduction of the unit cell size, followed by full geometry optimization, quickly leads to the formation of extended porous silicates, namely, silicates with cavities inside the structures (see Sil-1_4 and Sil-2_4 structures in Figures 1, 2). Indeed, in both systems, the nanocluster replicas interact along the three periodic directions in such a way that a cavity between them is created. These pores have diameters of ≈7–8 Å, which is a suitable size to encapsulate small gaseous molecules. Thus, if the protosilicate nanoclusters were capable to possess adsorbed molecules on their surfaces, they could potentially be retained during the aggregation process and finally become confined inside the formed porous.

Further reduction of the unit cell size leads to the formation of dense silicates (see e.g., Sil-1_6) with no pores. Interestingly, these compressed systems appear to be totally amorphous materials since the atomic positions do not seem to follow any regularity in space. This amorphous nature will be further explored by their simulated IR spectra (see below).

The relative energy of these “generated + optimized” systems with respect to that of the forsterite bulk Mg$_2$SiO$_4$ crystal (considered here as our reference system) as a function of system density is reported in Figure 3. The values of these energies are also reported in Table 2. Values are normalized with respect to the four Mg$_2$SiO$_4$ units present in the crystalline unit cell. The energy plots can also be understood as the energy variation of the systems with respect to the distance between proto-silicate units, where a high density implies a smaller inter-silicate distance and vice versa.

Among the different silicates studied here, crystalline forsterite is the most stable one, while the molecular nanocluster is the least stable. This is not surprising as: (i) for extended systems crystalline structures tend to be more stable than amorphous ones, and (ii) nanoclusters have a high percentage of undercoordinated surface atoms resulting in highly reconstructed and strained non-crystalline structures (Escatllar et al., 2019), leading to large instabilities. In our case, the isolated Mg$_6$Si$_3$O$_{12}$ nanocluster is approximately 390 kcal mol$^{-1}$ higher in energy than crystalline bulk Mg$_2$SiO$_4$.

For periodic structures without interactions between replicas, their energetic stability is, as expected, the same as the Mg$_6$Si$_3$O$_{12}$ nanocluster. Once interaction between clusters begins, the relative energies of the system with respect to forsterite decreases. For the first interacting systems, relative energies are still relatively high (330–345 kcal mol$^{-1}$), as the interaction is limited to a strained (MgO)$_2$ ring. However, for the subsequent increasingly interacting systems, relative energies significantly drop: the porous silicates lie 170–200 kcal mol$^{-1}$ above the energy of forsterite and the corresponding relative energies our densest silicates are <100 kcal mol$^{-1}$.

In the plots in Figure 3, the relative energies of compressed systems without optimized unit cell parameters are also represented (gray triangle points). The arrows indicate the resulting structures when full optimization (i.e., atomic positions + cell parameters) was performed from those without optimizing the unit cell. These later structures are more energetically unstable than their optimized unit cell analogues as the constrained cell parameters lead to artificially overly compressed structures which exhibit high geometrical strains. Therefore, we do not consider these systems as representative.
TABLE 2 | Relative energies (in kcal mol\(^{-1}\)) of the periodic silicate structures shown in Figures 1, 2 with respect to the bulk forsterite Mg\(_2\)SiO\(_4\) crystal (per unit formula).

| Figure 1 | Rel. E | Figure 2 | Rel. E |
|----------|--------|----------|--------|
| Sil-0    | 390.5  | Sil-0    | 390.5  |
| Sil-1\(_1\) | 388.4  | Sil-2\(_1\) | 388.4  |
| Sil-1\(_2\) | 381.8  | Sil-2\(_2\) | 381.8  |
| Sil-1\(_3\) | 345.7  | Sil-2\(_3\) | 327.8  |
| Sil-1\(_4\) | 205.8  | Sil-2\(_4\) | 168.0  |
| Sil-1\(_5\) | 135.1  | Sil-2\(_5\) | 67.9   |
| Sil-1\(_6\) | 82.8   | Sil-2\(_6\) | 66.0   |
| Sil-1\(_1\)\(^{\dagger}\) | 224.5  | Sil-2\(_1\)\(^{\dagger}\) | 261.8  |
| Sil-1\(_6\)\(^{\dagger}\) | 289.5  | Sil-2\(_6\)\(^{\dagger}\) | 196.9  |
|           |        | Sil-2\(_6\)\(^{\dagger}\) | 199.0  |

Their representation as a function of the corresponding densities is shown in Figure 3.

\(^{\dagger}\) These structures (not shown in Figures 1, 2) derive from optimizations in which the unit cell parameters were fixed.

Analysis of Simulated IR Spectra

Figure 4 shows the simulated IR spectra associated with the silicate structures reported in Figures 1 (black spectra) and 2 (red spectra), while Table 3 reports the calculated intensities and the vibrational mode assignment of the IR bands presented in Figure 4. For the sake of comparison, IR data related to the crystalline Mg\(_2\)SiO\(_4\) forsterite is also included. In Figure 4, gray shading indicates the positions of the IR bands for general interstellar silicates obtained from astronomical observations, which are centered at ca. 1,000 cm\(^{-1}\) and ca. 550 cm\(^{-1}\). The IR spectra of the molecular nanocluster and the crystalline bulk are also available in the literature (Navarro-Ruiz et al., 2014b; Martínez-González et al., 2018; Escatllar et al., 2019).

The forsterite spectrum shows a set of well-defined, relatively sharp IR bands (Figure 4g). Bands peaked between 1,000 and 800 cm\(^{-1}\) are assigned to the \(\nu\)(Si-O) stretching modes, those between 600 and 500 cm\(^{-1}\) to \(\delta\)(O-Si-O) bending modes, those around 400 cm\(^{-1}\) to rotational motions of the SiO\(_4\) tetrahedra, and those around 350 cm\(^{-1}\) to translational motions of the metal cations. In contrast, the IR spectrum of the Mg\(_6\)Si\(_3\)O\(_{12}\) nanocluster (Figure 4a) displays a wider variety of bands. This is due to the nanocluster’s lack of internal symmetry, which splits the IR bands into several signals because of the non-equivalent vibrations of the moieties. Despite this, IR assignments can also be grouped in a similar way as the crystalline ones.

In relation to the progressively reduced silicates, the IR spectra of the periodic non-interacting replicas systems (Sil-1\(_2\) and Sil-2\(_2\) of Figures 1, 2, respectively) are, expectedly, almost identical than that of the molecular nanocluster (compare spectra of Figure 4a with b). Changes start when the replicas of adjacent cells start to interact (Sil-1\(_3\) and Sil-1\(_4\) of Figure 1, and Sil-2\(_3\) and Sil-2\(_4\) of Figure 2). Because of the presence of the newly formed Mg-O bonds, some new bands assigned to the \(\nu\)(Mg-O) appear; in particular, the bands around 1,000 cm\(^{-1}\) (see spectra of Figures 4c,d), which were lacking in the non-interacting-replicas systems. The presence of these new bands converts the IR profiles into a more continuous band through the 1,200–800 cm\(^{-1}\) range. Due to this, the regions between the stretching vibrations and the rest of vibrations are more clearly differentiated in two broad bands. Such a differentiation is even more defined in the periodic fully interacting-replicas systems (i.e., Sil-1\(_5\) and Sil-1\(_6\) of Figure 1 and Sil-2\(_5\) and Sil-2\(_6\) of Figure 2). For these
TABLE 3 | Calculated frequencies and intensities, and assignment of the corresponding vibrational modes of the IR bands for the studied systems.

| System | Frequency (cm$^{-1}$) | Intensity (km/mol) | System | Frequency (cm$^{-1}$) | Intensity (km/mol) | Vibrational mode |
|--------|----------------------|--------------------|--------|----------------------|--------------------|------------------|
| Sil-0  | 1,109 159.5          | v(Si-O)            | Sil-1_3| 1,105 140.9          | 1,105 150.5        | v(Si-O)           |
|        | 915 202.3            | v(Si-O)            | Sil-1_4| 1,078 170.5          | 1,159 165.0        | v(Si-O)           |
|        | 852 145.5            | v(Si-O)            | Sil-1_5| 1,086 119.3          | 1,118 101.2        | v(Si-O)           |
|        | 749 142.7            | v(Si-O)            | Sil-1_6| 984 180.4            | 944 277.2          | v(Si-O)           |
|        | 579 455.6            | t(O-Si-O)          |        | 903 118.3            | 879 211.4          | v(Si-O)           |
|        | 397 419.5            | t(O-Si-O)          |        | 730 120.9            | 839 218.1          | v(Si-O)           |
|        | 321 401.5            | Transl. Mg         |        | 598 375.8            | 645 219.9          | v(Mg-O)           |
|        | 221 484.9            | Transl. Mg         |        | 536 387.4            | 495 435.3          | t(O-Si-O)         |
|        |                      |                    |        | 427 310.5            | 427 480.3          | t(O-Si-O)         |
|        |                      |                    |        | 334 183.0            | 271 550.3          | Transl. Mg        |
|        |                      |                    |        | 252 120.7            | 147 311.2          | Transl. Mg        |
| Sil-1_2| 1,095 180.4          | 1,097 207.5        | 252 120.7| 151 481.6          | 800 cm$^{-1}$ and between 1,100 and 800 cm$^{-1}$ (see spectra of Figures 4e,g). These IR features are in good agreement with those of large amorphous silicate models (Martínez-González et al., 2018) and observational measurements (Henning, 2010). In view of these results, the first interacting-replicas systems (Sil-1_3, Sil-1_4, Sil-2_3, and Sil-2_4) can be considered as transient states involved in the aggregation processes from proto-silicate nanoclusters to amorphous silicates.

It is finally worth mentioning that the superimposition of the two sets of spectra shown in Figure 4, from the Sil-1 and Sil-2 aggregation, although having different initial conditions, tend to produce bulk amorphous silicates with very similar IR profiles. This is an important fact because is suggests that, irrespective of the detailed route of the aggregation process, the resulting structures arising from each aggregation process are very similar observationally.
CONCLUSIONS

In this work we investigate theoretically the aggregation of proto-silicate nanoclusters (i.e., small silicate clusters) as a way to form interstellar silicate grains. The study is performed by means of periodic quantum mechanical simulations using DFT based calculations employing the hybrid B3LYP functional; a method known to be reliable for modeling silicate systems.

Using a stable Mg$_6$Si$_3$O$_{12}$ nanocluster as initial guess structure to form silicate aggregates, the adopted strategy to simulate the aggregation process is based on the progressive reduction in size of a 3D periodic unit cell centered on the nanocluster. Upon decreasing the lattice parameters, the nanocluster replicas in adjacent unit cells start to interact to form extended Mg$_2$SiO$_4$ silicate materials with progressively increasing density.

Our results indicate that the first interaction between nanocluster replicas place between Mg and O atoms, forming (MgO)$_2$ rings. These tenuously linked intermediate-aggregated systems exhibit internal cavities rendering them as nanoporous materials. Further reduction in size of the periodic box gives rise to systems in which the porosity disappears, leading to dense amorphous materials.

Energetic analysis of the resulting structures shows that all of them lie higher in energy than the forsterite Mg$_2$SiO$_4$ crystal bulk. The most unstable system is the isolated Mg$_6$Si$_3$O$_{12}$ proto-silicate nanocluster (ca. 400 kcal mol$^{-1}$ with respect to forsterite per formula unit). Once proto-silicate replicas start to interact, corresponding relative energies significantly decrease. For the non-interacting cases additional bands arise. For the interacting cases two very broad bands at 1,100–800 cm$^{-1}$ are exhibited. These bands are representatives of the amorphous nature of the structures and match fairly well with the astronomical IR observational. Interestingly, irrespective of the detailed proto-silicate aggregation processes, the resulting dense silicate structures show similar IR features, indicating that they are observationally very similar.

In summary, our results provide evidence that formation of interstellar silicate grains through proto-silicate aggregation is a feasible process, since the aggregation steps are energetically favorable and the final amorphous systems exhibit IR properties in fair agreement with those obtained observationally.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author/s.

AUTHOR CONTRIBUTIONS

All authors participated in the initial conception of the research idea and in the discussion of the results. AR did the quantum chemical simulations and participated in the writing and editing of the manuscript. SB participated in the writing and editing of the manuscript.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fspas.2021.659494/full#supplementary-material

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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