Scaling relation between genome length and particle size of viruses provides insights into viral life history

Highlights

- Capsid and genome size allometric exponent gives insights into viral life history
- The allometric exponent of NCLDV is almost twice that of bacteriophages
- The exponent is largely shaped by the viral entry mechanism and capsid stability
- The relaxed genome size constraint allows large viruses to evolve greater autonomy

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Scaling relation between genome length and particle size of viruses provides insights into viral life history

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SUMMARY

In terms of genome and particle sizes, viruses exhibit great diversity. With the discovery of several nucleocytoplasmic large DNA viruses (NCLDVs) and jumbo phages, the relationship between particle and genome sizes has emerged as an important criterion for understanding virus evolution. We use allometric scaling of capsid volume with the genome length of different groups of viruses to shed light on its relationship with virus life history. The allometric exponents for icosahedral dsDNA bacteriophages and NCLDVs were found to be 1 and 2, respectively, indicating that with increasing capsid size DNA packaging density remains the same in bacteriophages but decreases for NCLDVs. We argue that the exponents are largely shaped by their entry mechanism and capsid mechanical stability. We further show that these allometric size parameters are also intricately linked to the relative energy costs of translation and replication in viruses and can have further implications on viral life history.

INTRODUCTION

Viruses are obligate intracellular parasites that infect most cellular organisms in the biosphere. The simplicity of their makeup allows them to adapt and evolve rapidly to infect different life forms. They lie in a disconcerting line between the living and the nonliving. A convincing argument on the origin and diversification of viruses remains elusive. Owing to the lack of features that are key to life, such as energy generation, viruses have not found a place in the universal tree of life (Woese et al., 1990). But with the discovery of several new lineages of large complex viruses and the availability of viral genomic information, this paradigm is being reconsidered (Boyer et al., 2010; Koonin and Starokadomskyy, 2016; Forterre, 2017).

The life history of viruses includes traits, such as mode of transmission, replication rate, virus size, and burst size, that directly influence survival and reproduction (De Paepe and Taddei, 2006; Goldhill and Turner, 2014). Viruses exhibit great diversity in the type and size of their genetic material as well as the size and shape of the virus particle. The genetic material can be either single or double-stranded DNA or RNA. While the smallest virus has a genome of only 1.8 kb (single-stranded DNA genome of Circoviruses) (Finsterbusch and Mankertz, 2009), the largest virus (Pandoravirus) carries a 2.5-Mb double-stranded DNA genome (Philippe et al., 2013). Similarly, particle size can vary by up to four orders of magnitude (King et al., 2011; Cui et al., 2014). The study of size as an independent variable is a neglected area in virology. The recent discoveries of giant viruses have established size as an important ecological parameter that can have an influence on the life history of some viruses (Edwards et al., 2021).

Giant viruses are part of a diverse group of monophyletic viruses known as nucleocytoplasmic large DNA viruses (NCLDVs) (Iyer et al., 2001). The NCLDV order belongs to the newly established phylum Nucleocytoviricota (Koonin et al., 2020; Schoch et al., 2020), and it includes seven families (Poxviridae, Asfarviridae, Iridoviridae, Ascoviridae, Phycodnaviridae, Mimiviridae, and Marseilleviridae) of viruses infecting a wide range of eukaryotes, from higher mammals to unicellular protozoans (Colson et al., 2013). Other
unclassified giant viruses considered in the study are Mollivirus (Legendre et al., 2015; Christo-Foroux et al., 2020), Pandoravirus (Philippe et al., 2013; Legendre et al., 2018), Pithovirus (Legendre et al., 2014), Cedravirus (Andreani et al., 2016; Bertelli et al., 2017), Orpheovirus (Andreani et al., 2018), Faustovirus (Reteno et al., 2015; Benamar et al., 2016), Pacmanivirus (Andreani et al., 2017), Mininucleovirus (Subramaniam et al., 2020), and Medusavirus (Yoshikawa et al., 2019). Most NCLDV s are icosahedral viruses, while some such as Pandoravirus, Cedravirus, Pithovirus, and Orpheovirus are oval-shaped.

While most bacterial viruses carry genomes smaller than NCLDV s, some phages, known as jumbo phages, possess genomes of >200 kb (Yuan and Gao, 2017). Bacteriophage G, which infects Bacillus megaterium, is the first jumbo phage isolated and sequenced (genome size 498 kb, diameter 160 nm [Donelli, 1968; Donelli et al., 1975; Hua et al., 2017]). Other phages infecting B. megaterium have genome size in the range of 40–170 kb (Mihara et al., 2016). The burst size of jumbo phages ranges from 5 to 30 (Sharma et al., 2019), which is significantly less compared with other classical bacteriophages such as lambda and T4. Because viral burst size is a key fitness parameter, the smaller burst size of jumbo phages suggests higher viability of their progeny. Furthermore, comparative genomics showed that jumbo phages are phylogenetically different from the other phages, indicating their parallel evolution (Hua et al., 2017; Yuan and Gao, 2017).

Thus, there appears to be a greater degree of genome and particle size variation in both prokaryotic and eukaryotic viruses. While hosts are known to influence viral physiology, factors that play important roles in shaping these two important viral parameters, namely, particle size and genome size, have not been understood. In this study, we investigate how the size of viruses, especially large size (of both particle and genome), manifests in relation to their life history within its host. We also endeavor to gain insights into the possible evolutionary pressures exerted on the viruses by the competing organisms in the environment and the propellants of size diversity across NCLDV families. Although such an analysis based on two variables is coarse-grained, it serves to fill important gaps in understanding the characteristics influencing the life history of viruses.

RESULTS AND DISCUSSION

The relationship among all viruses (capsid volume, genome size, gene number) and their hosts

V iruses exhibited a wide range of distribution with both genome size and capsid volume (Figure 1). If all the viruses are considered, irrespective of the host, there appears to be a linear relationship between the external capsid volume and genome length with an exponent of 1.13 (p value < 2.2 × 10⁻¹⁶, \(R^2 = 0.67\)) when plotted on a log-log scale of base 10. There is no clear demarcation of either capsid or genome size range as per the host as each host can get infected by viruses of different sizes. An exponent of more than one suggests an out-of-proportion increase in the capsid volume compared with the genome length that implies a lesser packaging density for viruses with bigger capsids. A previous study determined the exponent with 88 viruses to be around 1.4 without considering the identity of the host (Cui et al., 2014), drawing a conclusion that prediction of virion size is possible from genome length using a simple scaling law. Here, we reexamine the relationship with a larger data set of 381 viruses (Table S1) and update the exponent (see Figures S1 and S2, and Table S2).

Genome size and capsid volume do not appear to scale proportionally in the case of RNA viruses when compared with the DNA viruses (Figure 1). Capsid volume variation of RNA viruses is about three orders of magnitude, while their genome size varies by about an order of magnitude. This variation in the physical parameters appears to be intricately linked to the life history traits of viruses (multiplication rate, viability, and mode of transmission/entry into host cell) that are ultimately related to their life cycle. In most RNA viruses, the inherent error-prone replication without proof-reading imposes a constraint on the genome size (Wellehan et al., 2016). In addition, there appear to be two mechanistically different pathways for capsid assembly in RNA viruses that could influence the capsid size (Perlmutter et al., 2014; Chevreuil et al., 2015). While the first mechanism involves a rapid, disordered, and random binding of capsid monomers to genomic RNA followed by rearrangements and ordering of capsid, the second pathway starts with the nucleation of capsid protein around the genomic RNA and its sequential growth leading to the completion of the assembly. In both mechanisms, the secondary and tertiary structure of the RNA genome and the preferred curvature of the assembled capsid emanating from the specific protein-protein interactions appear to influence the capsid size (Perlmutter et al., 2013; Beren et al., 2017). Thus, the dependence of the capsid size on the secondary and tertiary structure of the genomic RNA, along with its genome length (Hu et al., 2008), could possibly explain the wide variation of capsid volume in RNA viruses.
viruses (Figure 1). While the largest RNA virus has a genome size of 33.5 kb (Nidovirus), the average size appears to be about 10 kb (Saberi et al., 2018). In the case of RNA viruses, the exponent was 1.95 but the R^2 value was low (0.39). The packaging densities of RNA viruses were not estimated as the genome volume could not be calculated with confidence.

About 197 of 381 (50%) viruses we considered are dsDNA viruses. Table 1 summarizes the hosts and exponents calculated for the group of dsDNA viruses. The p and R^2 values of archaea and invertebrate subgroups are not significant, which might be owing to the small sample size, making it difficult to comment on the relationship between particle size and genome size among these subgroups. Viruses infecting vertebrate and unicellular eukaryotes such as protozoan and algae exhibit a slope of greater than 1 with a p value of 1.07 × 10^{-13} and R^2 value of 0.87, while interestingly, bacteria infecting viruses exhibit a slope of less than 1 with a p value < 2.2 × 10^{-16} and R^2 = 0.67.

The dsDNA viruses showed an increase in gene numbers with increasing genome length. Particularly, giant viruses with larger genomes also exhibit coding densities similar to that of smaller viruses (Van Etten et al., 2010; Philippe et al., 2013; Bajrai et al., 2016) and hence code for a large number of genes (Figure 1). Among icosahedral dsDNA viruses, the data were subdivided into viruses infecting bacteria and viruses of the NCLDV family that mostly infect unicellular eukaryotes such as protozoan and algae. NCLDVs such as poxviruses that infect higher multicellular eukaryotes and other non-NCLDV eukaryotic dsDNA viruses such as herpesvirus, adenovirus, and so on were excluded from this study considering their wide host range (which led to different life histories) and host cell size. Bacteriophages are the most studied group of viruses, facing different environments and evolutionary pressures to those faced by NCLDVs that infect protozoan or algae. Hence, a comparative study of these two subsets will serve as a base to understand the evolution of these viruses.

**The allometric relationship between genome length and particle size of icosahedral dsDNA bacteriophages and NCLDVs**

The regression gives an exponent of about 0.95 for the bacteriophage subgroup with an R^2 value of 0.70 and a significant p value (<2.2 × 10^{-16}). The exponent from the regression line of NCLDVs is 2.00, with
The exponents of these subgroups (0.95 and 2.00) fall on either side of the regression line exponent of viruses across different hosts (1.13) (Figure 2). The exponent values suggest that in the case of bacteriophages both the parameters are increasing in proportion with each other, while in NCLDVs, the capsid volume is increasing at a much higher magnitude than their genome length. Consequently, the genome packaging density of NCLDVs is lesser compared to the bacteriophages.

We hypothesize that the particle size and genome size intersect at two stages in the virus life cycle. The first is when a virus enters the host cell, and the second is during genome packaging and capsid assembly. The mode of entry might have a huge impact on the optimization of particle and genome sizes of viruses. Capsids less than a threshold size cannot accommodate large genomes, while smaller genomes may not create enough internal pressure inside the capsid required for genome injection, which is inevitable for successful infection by most bacteriophages (Nurmemmedov et al., 2007). The NCLDVs, on the other hand, appears to have no such prerequisite for infection, as whole virus particles enter the host cell by either phagocytosis or endocytosis, eliminating the role of viral packaging density on their infection capability.

Although dsDNA bacteriophages exhibit size variability, an overwhelming majority of them (~85%) have an icosahedral structure (Ackermann, 2003). Amoeba-infecting giant viruses, on the other hand, appear to have a far more diversity in shape, including spherical, icosahedral, ovoidal, and icosahedron with a tail. This points to a lack of evolutionary pressure on the shape of giant viruses, whereas icosahedral bacteriophages do not have the same independence to change their shape. A simulation study on semiflexible polymers showed that sphere-shaped capsids package and eject genome at a much faster rate (Ali et al., 2006). Icosahedron, being similar to a sphere where pressure is exerted upon the genome from all sides facilitating genome injection into the host, might be as per bacteriophages to maintain their infectious capacity.

Giant viruses enter the amoebal host by phagocytosis. Because amoeba appears to indiscriminately engulf and phagocytose particles of size 0.5 µm or greater (Korn and Weisman, 1967; Raoult and Boyer, 2010), it appears that capsid size—rather than its shape and internal capsid pressure (see the next section)—is critical for infection. Because amoeba harbors a gamut of microbes such as bacteria, viruses, algae, and fungi, the larger particle size of giant viruses might have resulted from the competition with microorganisms to be phagocytosed (Slimani et al., 2013). Furthermore, genetic recombination events with other microbial genomes in the amoebal “melting pot” could have led to the size expansion of giant viral genomes (Boyer et al., 2009; Colson and Raoult, 2010). Giant viruses have been shown to accumulate genes that encode repeat-domaining proteins (Shukla et al., 2018), transpovirions, and provirophages in high copy numbers (Desnues et al., 2012). While the larger of the giant viruses such as Mimivirus, Pithovirus, Pandoravirus, and so on enter the host cell by phagocytosis, the smaller Marseillevirus that has a capsid of only about 250 nm in diameter has evolved to enter via pinocytosis or by phagocytosis of aggregates of several viral particles (Arantes et al., 2016). Such variation in the entry mechanism is not observed in icosahedral bacteriophages.

### Packaging density of dsDNA icosahedral bacteriophages and NCLDVs

Although the scaling exponents provide us great insights into how the capsid size evolves with genome size, they do not directly inform us about how tightly the DNA is packaged within the viral capsids and

### Table 1. Power law fit, $y = ax^m$, for capsid volume ($y$) and genome length ($x$) for each group of dsDNA viruses classified as per their host

| Host            | No of dsDNA viruses | $m$    | $A$    | $R^2$ | $p$ value   |
|-----------------|---------------------|--------|--------|-------|-------------|
| Vertebrates     | 29                  | 1.25   | 3.88   | 0.87  | $1.07 \times 10^{-13}$ |
| Invertebrates   | 13                  | 2.49   | 0.67   | 0.34  | 0.02        |
| Bacteria        | 106                 | 0.87   | 3.70   | 0.66  | <2.2 $\times 10^{-16}$ |
| Archaea         | 15                  | 0.58   | 4.61   | 0.09  | 0.15        |
| Protozoans, algae | 33                 | 1.96   | 1.71   | 0.70  | 5.37 $\times 10^{-10}$ |

Allometric exponents $m$, proportionality coefficient $A$ and the associated statistical parameters ($R^2$ and $p$ value) for linear regression of the form $Y = mX + A$, where $Y = \log y$ and $X = \log x$ and $A = \log a$ to the data for different hosts. All logs are to the base 10. See also Figure S1A.
its possible connection with the viral infection mechanism. It is well-known from the literature that the so-called pressure within the viral capsids is related to the spontaneous ejection of DNA from the viral capsid during infection (Evilevitch et al., 2003; Tzlil et al., 2003). Bacteriophages infect the host by injecting their DNA into the host, while the capsid stays outside. On the other hand, NCLDVs bring about host infection by phagocytosis in which the entire virus is ingested into the host. Hence, it is reasonable to expect that the internal pressure inside the phage capsid is generally higher than that within NCLDVs. Because it is known from the literature that the pressure within the capsid increases with packaging density (Rau et al., 1984; Purohit et al., 2005; Bauer et al., 2015), we hypothesize that statistically speaking, the packaging density within bacteriophages should be greater than that in the NCLDVs. Indeed, from our data (see STAR methods and Figure S3), we find that the median value of the DNA packing fraction within the dsDNA icosahedral phages is approximately 0.47 (standard deviation – 0.23) as compared with the much lower value of 0.09 (standard deviation – 0.14) for dsDNA icosahedral/spherical NCLDVs. Thus, our study gives us another potential connection between viral allometry (packing density) and life history (infection mechanism).

The “overlapping region”

Another unexpected finding from our studies comes from exploring the “overlapping region” between bacteriophages and NCLDVs in Figure 2. Although on average, the allometric relation between the bacteriophages and NCLDVs is quite different, owing to statistical fluctuations a few data points from smaller NCLDVs and larger bacteriophages (or jumbo phages) seem to be mixed in this region. This prompted us to ask a very naive question: given this overlap, are there also any similarities between jumbo phages and smaller NCLDVs? Surprisingly, we found that jumbo phages have an ancestry that is significantly branched off from both smaller bacteriophages and NCLDVs (Yuan and Gao, 2017). Interestingly, jumbo phages have a few important life-history traits that are remarkably similar to those of NCLDVs. For example, jumbo phages, unlike smaller bacteriophages, are believed to maintain viral factory-like structures during their life cycle (Chaikertasik et al., 2017). Compartimentalization helps bigger viruses to protect their genome from antivirals and nucleases as well as replication and transcription processes take place efficiently by concentrating required factors. Moreover, similar to NCLDVs, jumbo phages have more genes...
associated with genome replication and nucleotide metabolism, as compared with smaller phages (Yuan and Gao, 2017). On the other front, smaller NCLDVs, which are typically algae-infecting viruses, have life-history traits that also show certain similarities with bacteriophages. For example, during infection, Paramecium bursaria chlorella virus (a member of the Phycodnaviridae family that infects the unicellular green alga Chlorella sp.), such as bacteriophages, only inject its DNA into the host while leaving the capsids outside (Van Etten, 2003). Similarly, some of these viruses also exhibit pseudolysogeny (Van Etten et al., 1991; Thomas et al., 2011), which is a common phenomenon observed in bacteriophages that helps in the long-term survival of viruses in unfavorable environments (Abedon, 2008). These observations suggest that though the phylogeny of bacteriophages and NCLDVs are divergent, virus size in itself could influence the life-history traits of viruses.

**Potential implications of values of \( m \) in the relation \( V_c \sim L_g^m \) for viral life history**

From Figure 2, we obtained that the viral capsid volume \( V_c \) is connected to the packaged genome length \( L_g \)

\[
V_c \sim L_g^m, \quad (Equation \ 4)
\]

where the exponent \( m \approx 1 \) for phages and \( m \approx 2 \) for NCLDVs. Because \( V_c \sim r_c^3 \), where \( r_c \) is the capsid inner radius, Equation 4 can be re-written as

\[
r_c \sim L_g^{m/3}. \quad (Equation \ 5)
\]

The difference in the \( m \) values of phages and NCLDVs leads to interesting implications as discussed in the following text.

**Implication of \( m \) for viral capsid stability**

As discussed earlier in the section on DNA packaging density, the pressure in the viral capsid is generally an increasing function of DNA packaging density (Rau et al., 1984; Purohit et al., 2005; Bauer et al., 2015). Hence, the effective internal pressure in the capsid is as follows:

\[
p_c(\rho) = \rho_c \left( L_g / r_c^3 \right), \quad (Equation \ 6)
\]

where, \( \rho_c \) is an increasing function of its argument. We use the same symbol \( \rho_c \) in both sides of Equation 6 for notational economy. Using Equations 5 in 6, we get that \( p_c(\rho) = \rho_c \left( r_c^{1+3} \right) \). It is known that tangential tension is generated in the walls of spherical pressure vessels (also called as hoop stress) due to internal pressure (Barber, 2010). By modeling the virus as one such with internal pressure \( p_c \), we can obtain the tensile stress in the viral capsid walls as \( \sigma = p_c r_c / t = \rho_c \left( r_c^{1+3} \right) r_c / t \) using simple mechanical considerations, where \( t \) is the thickness of the capsid and \( t \ll r_c \) (thin walls) (Barber, 2010). For the capsid to remain intact and not burst, the tensile stress \( \sigma \) should be less than the ultimate tensile strength \( \sigma_u \) of the capsid walls. Hence,

\[
\sigma_u > \sigma = p_c \left( r_c^{1+3} \right) r_c / t. \quad (Equation \ 7)
\]

We see from this simple expression that the tensile stress increases with size for the same amount of internal pressure.

During capsid self-assembly, high mechanical stresses could be generated in the capsid surface owing to a combination of growth and Gaussian curvature. This stress could be relieved by creating topological defects in the icosahedral capsid surface or by inducing anisotropy in its growth and creating elongated capsids (Castelnovo, 2017). However, it is known from theoretical considerations, numerical simulations, and experiments that viral capsids still retain residual stress (Klug et al., 2012; Zandi et al., 2020). In our simple calculation, we take the residual stress in the capsid as a given, and the pressure created by the packaged DNA simply adds tensile stress (Equation 7) to the capsid. It was shown in a numerical study that for viral capsids with higher triangulation number \( T \), the residual tension at the hexamer locations is high, though the increase in tension with \( T \) is not always monotonic (Zandi and Reguera, 2005). Similarly, it is also observed that the size of individual capsomeres is very similar for different viruses. In that case, \( T \sim r_c^6 \).
where $\alpha \approx 0.5$, that is, capsid $T$ number increases with increasing capsid radius (Božič et al., 2013). Thus, the residual stress in the capsid at some locations should generally increase with the capsid size. The study of intricate details of force generation in the capsid owing to a combination of DNA pressure and capsid self-assembly residual stresses is beyond the scope of this article. However, the residual tension could reduce the effective ultimate tensile strength of the capsid walls $\sigma_d(r_c)$ (Zandi and Reguera, 2005), which, from the aforementioned discussion, is expected to decrease with $r_c$. Because $m \approx 1$ in the case of bacteriophages, for capsid integrity $\sigma_d(r_c) > \frac{\mu}{2}\Delta u_0$, where the term $\mu(1)$ indicates that the capsid pressure varies little with phage size. Hence, as the capsid size increases, the capsid wall stress increases with $r_c$, while its ultimate tensile strength $\sigma_d(r_c)$ decreases, making the capsid failure-prone. Indeed, jumbo phages have decoration proteins that are known to provide structural strength to the capsid (Effantin et al., 2013). However, the production of decoration proteins should require additional resources from the host and increased information in the viral genome.

For NCLDVs, $r_c$ increases to sizes that are up to three times the size of jumbo phages. As a result, for the same internal pressure $p_e$, as for the phages, the capsid wall stress will increase many folds, on the one hand, while $\sigma_d$ keeps decreasing on the other. Hence, the reinforcement requirement for sustaining capsid integrity would increase many times when compared to even jumbo phages. However, it seems that NCLDVs have evolved another strategy to counter the threat of structural failure. In their case, because $m = 2$, the structural integrity condition becomes $p_e(r_c^{-3/2}) < \frac{\mu}{2}$. Hence, the integrity condition could be satisfied because, while the term on the right-hand side decreases with increasing capsid size, as discussed previously, the pressure $p_e(r_c^{-3/2})$ on the left-hand side, unlike for phages, also simultaneously decreases. As a result, NCLDVs could maintain their capsid integrity with respect to internal pressure owing to the genome. Thus, the scaling exponent $m = 2$ in $V_c \sim L_g^m$ could have this important implication for NCLDVs.

**Implication of allometric exponent $m$ for metabolic cost of viral life history**

DNA replication and translation of capsid proteins are two of the most energy intense events in viral life history (Mahmoudabadi et al., 2017). As discussed in the previous subsection, assuming that the capsomere sizes remain approximately constant across different viruses, the number of capsid proteins $N_c \sim r_c^2$, the approximate area of the capsid surface (Mahmoudabadi et al., 2017). Hence, the energy cost of translating capsid protein(s) for a single virus (Mahmoudabadi et al., 2017) scales as

$$E_{tl} \sim r_c^2.$$  
(Equation 8)

Similarly, because the energy cost of replicating DNA of a single virus $E_{rep} \sim L_g$ (Mahmoudabadi et al., 2017), using Equation 5, we get that

$$E_{rep} \sim r_c^{3/m}.$$  
(Equation 9)

As seen before, $m = 1$ for bacteriophages, owing to which $E_{rep} \sim r_c^1$. Hence, when $r_c$ is small, the translation cost $E_{tl} \sim r_c^2$ is expected to dominate over the replication cost $E_{rep} \sim r_c^1$. The reverse should be true when the size $r_c$ of virus increases (Mahmoudabadi et al., 2017), especially for NCLDVs as they have large capsid sizes compared with most bacteriophages. Hence, if the same $m = 1$ for bacteriophages were applicable for NCLDVs, we would expect $E_{rep}$ to dominate over $E_{tl}$ for these viruses. However, as seen earlier, for NCLDVs $m = 2$, owing to which $E_{rep} \sim r_c^{3/2}$, and the translation cost $E_{tl} \sim r_c^2$ should dominate over the replication cost for NCLDVs even for larger capsid sizes. The replication cost for NCLDVs in terms of $r_c$ can be obtained by using the scaling relation expressed in Equations 4 in 1. This scaling relation could be written more explicitly as $V_c = \frac{4}{3}\pi r_c^3 = aL_g^m$, from which $L_g = \left(\frac{4}{3}\pi r_c^{-3/m}\right)^{1/m}$.

The exponent $m = 2.00$ and the proportionality coefficient $a = 10^{1.38}$ were obtained for NCLDVs using the fitting procedure described earlier (see Figure 2 caption, STAR methods section). As expected, this relation well represents the energetic cost $E_{rep}$, as a function of capsid radius for NCLDVs (Figure 3).

What could be the potential implication of this finding for viral life history? According to Mahmoudabadi et al. (2017) and our arguments presented previously, the cost associated with making capsid proteins dominate the energy budget. The fact that protozoan and algal giant viruses exist in large numbers (Monier et al., 2008; Hingamp et al., 2013; Li et al., 2019) suggests that a bigger size is beneficial to viruses in certain host/environmental niches. Furthermore, the finding that many NCLDVs have independently evolved bigger sizes (Filee, 2013) suggests common evolutionary mechanisms of size expansion that are yet to be
understood. If the energy budget of the host is indeed a limiting factor in the case of bigger viruses, the number of progenies will have to be sacrificed. In this case, however, if the fitness of each virion increases, say, owing to an increase in virion stability because of low DNA packaging, as argued earlier (Edwards et al., 2021), then only a fewer of them are needed for continued sustenance. The larger size of the virion is also helpful for phagocytosis (Rodrigues et al., 2016). If the energy budget of the host is not a limiting factor, then all these considerations are still relevant but without the strict constraint on the progeny number.

What is the advantage of such big capsids for evolution? A larger capsid size can, in principle, help viruses accrue more genetic content. Because we have argued that the cost of DNA replication is a small fraction of the energy required for producing capsid protein(s), the cost burden of this acquisition is minimal. If, in addition, it does not affect the overall fitness of the virus, the newly acquired DNA can explore the evolutionary landscape via genetic drift. It was recently proposed that in the case of *Pandoravirus* (Legendre et al., 2019), some acquired noncoding DNA have transitioned to protein-coding ones *de novo*. Furthermore, the newborn genes were found to be under “slight” negative selection pressure indicating that they are in the process of fixation (Legendre et al., 2019). Thus, it appears that capsid expansion confers higher evolvability to some giant viruses in certain host niches leading to their diversification. In the process, giant viruses contribute novel genes to their environment via mobilomes in the protozoan “melting pot” (Desnues et al., 2012; Colson et al., 2017).

The two parameters of the virus, capsid radius $R_c$ and genome size $L_g$ have important implications for the life history of viruses. By increasing $L_g$, the virus can have greater complexity because its ability to translate more proteins increases. On the other hand, capsid volume $V_c \sim r_c^3$ provides a cap on how big their genome could be. Having a large packaging density $\rho \sim L_g/r_c^3$, loosely speaking, leads to higher internal pressure within the capsid which is widely believed to be used by bacteriophages to inject their DNA into the host cells during infection (Grayson et al., 2006; Brandariz-Nunez et al., 2019). However, large internal pressure combined with large capsid size could make the virus susceptible to mechanical failure by tearing of the capsid wall owing to tension. Hence, many large phages have decorating proteins and/or cementing proteins to safeguard against rupture. Manufacturing of these additional ingredients, nevertheless, require energy and
material resources from the host. The really large NLCDVs, however, are even more susceptible to capsid rupture. But as discussed previously, the fact that the DNA packaging density decreases with increasing size of NCLDVs could help reduce the internal pressure for larger viruses. Moreover, NCLDVs do not require high internal pressure to inject their genome into their protozoa host because they carry out the infection by entering into the host by phagocytosis. In fact, the large size of NCLDVs is comparable with that of many bacteria that are also ingested for nutrition by protozoa via phagocytosis. Hence, it is conceivable that the NCLDVs are well placed in terms of size for ingestion into their host.

Conclusion
In this study, by meticulously analyzing the capsid and genome sizes of a large number of viruses, we show that the allometric exponent between these two parameters gives us insights into the evolution and life histories of viruses. A major finding from this study is that the allometric exponent of NCLDVs is almost twice that of bacteriophages. In the case of bacteriophages, the need to maintain the internal capsid pressure, which is essential for infection, seems to impose a major constraint on genome evolution. On the other hand, the constraint on genome evolution seems to be relaxed in the case of many unicellular eukaryotes-infecting NCLDVs that have evolved larger capsids for a lesser amount of DNA (and hence exhibit a higher exponent) to suit their mode of infection while maintaining capsid stability. Consequently, larger capsids could potentially accommodate additional DNA without adversely affecting its energy budget. We propose that this feature has helped in the evolution of larger viruses with greater autonomy. Overall, we suggest plausible reasons for the interplay between genome and particle sizes as important life-history determinants of viruses.

Limitation of the study
While we have taken utmost care in gathering our data, there could be some variations in the capsid sizes (e.g. owing to pH conditions) and capsid thickness than the ones used in the article. These differences could produce some errors in the calculated DNA packaging density, especially for smaller capsids. Our findings regarding the allometric exponent and the associated implications are applicable in a statistical sense, and there are viruses within the group that do not follow the expected trend. Based on the literature, we take DNA replication and capsid protein production to have the highest energy costs for the virus. However, the energy cost for making other gene products could also be high, especially for NCLDVs. We implicate the tension in capsid walls owing to DNA packaging pressure to be a determinant of capsid mechanical stability. However, we could not account for environmental conditions, such as temperature and pH, that could modify interactions between capsomeres and be significant for capsid stability.

STAR METHODS
Detailed methods are provided in the online version of this paper and include the following:

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AUTHOR CONTRIBUTIONS

H.V.C., M.M.I., and K.K. conceived and designed the research. H.V.C. performed the research. All the authors analyzed the data and wrote the manuscript.

DECLARATION OF INTERESTS

The authors declare no competing interests.

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STAR★METHODS

KEY RESOURCES TABLE

| Resource                         | Source                      | Identifier       |
|---------------------------------|-----------------------------|------------------|
| Software and algorithms         |                             |                  |
| R Project for Statistical Computing | (Team, 2020)               | RRID:SCR_001905 |
|                                 |                             | [https://www.R-project.org/](https://www.R-project.org/) |
| R Package – ggplot2              | (Wickham, 2016)             | RRID:SCR_014601 |
| R Package – stats               | (Team, 2020)                | N/A              |
| R Package – dplyr                | (Wickham et al., 2015)      | RRID:SCR_016708 |
| R Package – xlsx                 | (Dragulescu and Arendt, 2012) | N/A              |
| Other                           |                             |                  |
| ViralZone Database              | (Hulo et al., 2011)         | RRID:SCR_006563  |
|                                 |                             | [https://viralzone.expasy.org/](https://viralzone.expasy.org/) |
| NCBI viral genomes resource     | (Brister et al., 2015)      | RRID:SCR_006472  |
|                                 |                             | [https://www.ncbi.nlm.nih.gov/](https://www.ncbi.nlm.nih.gov/) |

RESOURCE AVAILABILITY

Lead contact
Further information and requests for resources should be directed to and will be fulfilled by the lead contact, Dr. Kiran Kondabagil; Email ID: kirankondabagil@iitb.ac.in, Telephone Number: +91-22-25767758.

Materials availability
This study did not generate any new materials.

Data and code availability
Data sets used for this study are provided in the Table S1. The present research did not use any new codes.

METHOD DETAILS

Data collection
For this study, only viruses that infect all types of life forms were considered. Viruses such as virophages and satellite viruses that rely on other viral infections for their replication cycle were not considered. Data on genome type and length, capsid size, and shape of viruses were collected from ViralZone:[https://viralzone.expasy.org/](https://viralzone.expasy.org/) (Hulo et al., 2011) and NCBI databases:[https://www.ncbi.nlm.nih.gov/](https://www.ncbi.nlm.nih.gov/) (Brister et al., 2015). In the cases of some giant viruses and jumbo phages, data were also gathered from literature (references available in the Table S1). Information regarding the host type and entry mechanism was also collected from the literature. Data on genome sizes obtained from ViralZone were verified with the NCBI database. For viruses with a segmented genome, the total size of all segments was considered. To remove statistical redundancy, viruses with the same capsid and genome sizes were represented only once in the plot. Wherever the capsid size is denoted by a range, an average of the highest and lowest value was taken. Regardless of whether the virus is enveloped or nonenveloped or it has an irregular nucleocapsid, we used the representative values of capsid radius from the ViralZone database. Details of the parameters collected for all viruses including the type of genetic material are shown in the Table S1.

In the case of bacterial viruses, only the capsid head dimensions were used for estimating the capsid volume. The data for capsid size/shape and genome size were meticulously collected from a wide variety of sources. Although the errors in the genome size are expected to be negligible, there may likely be few errors in the measurement of capsid sizes, for example, owing to physiological conditions under which capsid sizes were measured, especially for smaller viruses (Figure S3). Although such discrepancies, in themselves, are small enough to be inconsequential, they make their presence felt in a few cases (around 5 of 85 dsDNA
icosahedral bacteriophages) where we find that the packing density of DNA in the viral capsids (as explained below in the section "Volume and packaging density calculation") turns out to be greater than one, something that is not possible unless the double helix of the DNA could itself be distorted during packaging. Hence, we remove such isolated cases (5 bacterial viruses) from our data set as their packaging ratio is greater than 1, which might be owing to errors in capsid dimensions. These are, however, isolated cases and are not expected to cause any significant modifications in scaling exponents.

Our final data set consisted of a total of 381 viruses – 114 bacterial, 69 plant, 100 vertebrate (52 human), 29 invertebrate, 11 algae, 32 protozoan, 8 fungal, and 18 archaeal viruses. The bacterial viruses considered included 29 jumbo phages.

QUANTIFICATION AND STATISTICAL ANALYSIS

Volume and packaging density calculation

In the case of icosahedral viruses, particle size was approximated from the capsid dimensions. For nonicosahedral viruses, capsid volume was estimated using the particle size parameters, namely, length, breadth, and height. The volume of capsid was calculated using different formulas for different shapes, spherical (icosahedral) viruses \( V = \frac{4}{3} \pi R^3 \), Ovoid (lemon-shaped) viruses \( V = \frac{4}{3} \pi a^2 c \), filamentous (rod) viruses \( V = \pi R_l^2 h \), and brick viruses \( V = h d l \). In these formulas, \( V \) is the virion volume, \( R_c \) is the capsid outer radius, \( a \) is the equatorial radius of the spheroid, \( c \) is the distance from center to pole along the symmetry axis, \( l \) is virion length, \( h \) is height, and \( d \) is depth. These formulas were also used in a previous allometry study (Cui et al., 2014).

For further analysis of the dsDNA icosahedral viruses subgroup considered (bacteriophages, jumbo phages, and NCLDVs), the capsid volume was corrected by considering the thickness of the capsid protein wall which was estimated to be about 3 nm in the case of bacteriophages (Bozić et al., 2013) and 10 nm in the cases with an internal lipid membrane, such as NCLDVs (Xiao et al., 2017; Okamoto et al., 2018; Yoshi-kawa et al., 2019). In the case of Mimivirus, the capsid is made up of 5 different layers, so the capsid thickness value was taken as 70 nm (Xiao et al., 2009), and in the case of Marseillevirus, the capsid is made up of a single lipid bilayer giving a capsid thickness of about 10 nm (Okamoto et al., 2018). For other NCLDVs, capsid thickness was taken as 10 nm considering that all are having a single lipid bilayer.

Packaging ratio for dsDNA icosahedral viruses was calculated as \( \frac{V_g}{V_c} \), where \( V_c \) is the capsid volume and \( V_g \) is the genome volume calculated as \( V_g = 0.34 \pi r + L_g \) by assuming DNA to be a cylinder of radius 1 nm and each base pair is separated by ~0.34 nm (Purohit et al., 2005) and \( L_g \) is the genome length in base pairs.

Data analysis

The statistical analysis was performed in R v4.0.3 (Team, 2020). Log-log plots were made using ggplot package. For linear regression fit, lm function from stats package was used. The xlsx and dplyr packages were used to read excel sheets and to subgroup the data, respectively.

Following the previous allometry study (Cui et al., 2014), we have classified the data to update the scaling relation between genome size and particle size as per (I) Baltimore classification: dsDNA \( (n = 197) \), ssDNA \( (n = 30) \), dsRNA \( (n = 26) \), ssRNA(-) \( (n = 88) \), ssRNA(+) \( (n = 26) \), reverse-transcribing (dsDNA \( [n = 8] \), ssRNA \( [n = 6] \)) \( (n = 14) \) (Figures S1A–S1F); (II) enveloped \( (n = 113) \) and nonenveloped viruses \( (n = 268) \), (Figure S2A & B); and (III) icosahedral viruses (including spherical) \( (n = 291) \) and nonicosahedral viruses (includes rod, ovoid, filamentous, prolate, brick) \( (n = 90) \) (Figures S2C and S2D). A comprehensive study of scaling relation in these subgroups is provided in the Table S2. For a detailed analysis of the impact of a host on the relationship between particle size and genome size, two subgroups of dsDNA icosahedral viruses, bacterial viruses \( (n = 80) \), and viruses infecting unicellular eukaryotes such as protozoan and algae were selected \( (n = 28) \).

Calculation of viral energetic cost

In their detailed analysis, Mahmoudabadi et al. (2017) calculated energy costs for making a virus from different viral life-cycle components and reported that genome replication and protein translation costs for capsid are the two most dominant ones. We use a similar approach as theirs to find the energy costs for the bacteriophages and NCLDVs.
Replication energy
Following Mahmoudabadi et al. (2017) the replication energy for the virus can be calculated directly using genome length $L_g$ in base-pairs as

$$E_{REP}(dsDNA)/v = 2(L_g)\left(e_d + e_p + e_{od}\right),$$

(Equation 1)

where, the single DNA nucleotide cost is taken as the sum of the average direct cost of DNA synthesis from precursor metabolites ($e_d$), the cost of chain elongation per base ($e_p$), and the average opportunity cost per nucleotide ($e_{od}$) (Mahmoudabadi et al., 2017). Multiplication by factor of 2 arises because of the double-stranded nature of the genome. The reported numerical values of various energy costs in Equation 1 are $e_p = 2$ ATP (Lynch and Marinov, 2015), $e_d = 11$ ATP, $e_{od} = 34$ ATP (bacterial host), and $e_{od} = 42$ ATP (eukaryote host). Values are taken from (Mahmoudabadi et al., 2017). More details about these issues are provided in the section on metabolic costs. Genome packaging in most large dsDNA viruses is accomplished by an ATP-driven packaging motor (Rao and Feiss, 2008; Sun et al., 2008; Chelikani et al., 2014). The cost of DNA packaging in bacteriophages ø29 and T3 was estimated to be about one ATP for every two base pairs of DNA translocated (Guo et al., 1987; Morita et al., 1993; Chemla et al., 2005). However, as can be seen from Equation 1, the replication cost per base pair of DNA is approximately 94 ATP (bacterial host) and 110 ATP (eukaryote host). Hence, as the DNA packaging cost is significantly lesser as compared to DNA replication energy cost, we do not include it in our calculations.

Similarly, by assuming that the viral capsid of radius $R_c$ is half filled with DNA (Jover et al., 2014), the DNA replication cost for the virus can also be obtained as follows:

$$E_{REP}(dsDNA)/v = \frac{4\pi r_c^3}{3v_d}(e_d + e_p + e_{od}).$$

(Equation 2)

Here, packaged genome length is obtained by dividing capsid inner volume by $v_d$ ($\approx 1$ nm$^3$) (Milo et al., 2010), the approximate volume of a single base pair and $r_c$ is the capsid inner radius.

TRANSLATION ENERGY
Following the study by Mahmoudabadi et al. (2017), we assume that the main cost of protein translation is associated with capsid proteins. Hence, for a virus with inner radius $r_c$,

$$E_{T}(dsDNA)/v = \frac{4\pi r_c^2 t}{v_a}(e_a + e_{aa} + e_{oa}),$$

(Equation 3)

where, $e_a$ is the average direct cost to produce amino acids from precursor metabolites, $e_{aa}$ is the cost of formation of each polypeptide bond, and $e_{oa}$ is the average opportunity cost per amino acid. Here, the number of amino acids is roughly obtained by dividing the capsid volume by $v_a$ ($\approx 0.1$ nm$^3$) (Counterman and Ciemmer, 1999), the approximate volume of an amino acid. The thickness $t$ of the capsid is taken as 3 nm for bacteriophages (Božić et al., 2013) and 10 nm for NCLDV s (Xiao et al., 2017; Okamoto et al., 2018; Yoshikawa et al., 2019). The numerical values for $e_{aa} = 4$ ATP (Phillips et al., 2012), $e_a = 2$ ATP, $e_{oa} = 25$ ATP (bacterial host), and $e_{oa} = 30$ ATP (eukaryotes host) (values are taken from Mahmoudabadi et al., 2017). Note that, because the protein copy numbers making up the capsid for most NCDLVs have not yet been elucidated, we cannot get the exact translation cost using actual number of amino acids. Hence, we resort to the approximation made in Equation 3.