The Fifth Catalogue of Nearby Stars (CNS5)

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ABSTRACT

Context. We present the compilation of the Fifth Catalogue of Nearby Stars (CNS5), based on astrometric and photometric data from Gaia EDR3 and HIPPARCOS and supplemented with parallaxes from ground-based astrometric surveys carried out in the infrared.

Aims. The aim of the CNS5 is to provide the most complete sample of objects in the solar neighbourhood. For all known stars and brown dwarfs in the 25 pc sphere around the Sun, basic astrometric and photometric parameters are given. Furthermore, we provide the colour-magnitude diagram (CMD) and various luminosity functions of the stellar content in the solar neighbourhood, and characterise the completeness of the CNS5 catalogue.

Methods. We compiled a sample of stars and brown dwarfs that are most likely located within 25 pc of the Sun, taking space-based parallaxes from Gaia EDR3 and HIPPARCOS as well as ground-based parallaxes from Best et al. (2021, AJ, 161, 42), Kirkpatrick et al. (2021, ApJS, 253, 7), and from the CNS4 into account. We developed a set of selection criteria to clean the sample from spurious sources. Furthermore, we show that effects of blending in the Gaia photometry, which mainly affect the faint and red sources in Gaia, can be mitigated to reliably place those objects in a CMD. We also assessed the completeness of the CNS5 using a Kolmogorov-Smirnov test and derive observational optical and mid-infrared (MIR) luminosity functions for the main-sequence stars and white dwarfs (WDs) in the solar neighbourhood.

Results. The CNS5 contains 5931 objects, including 5230 stars (4946 main-sequence stars, 20 red giants and 264 white dwarfs) and 701 brown dwarfs. We find that the CNS5 catalogue is statistically complete down to 19.7 mag in the G-band and 11.8 mag in W1-band absolute magnitudes, corresponding to a spectral type of L8. The stellar number density in the solar neighbourhood is (7.99 ± 0.11) × 10⁻² stars pc⁻³, and about 72% of stars in the solar neighbourhood are M dwarfs. Furthermore, we show that the WD sample in CNS5 is statistically complete within 25 pc. The derived number density of WDs is (4.03 ± 0.25) × 10⁻³ stars pc⁻³. The ratio between stars and brown dwarfs within 15 pc is 4.6 ± 0.4, whereas within 25 pc it is 7.5 ± 0.3. Thus, we estimate that about one third of brown dwarfs are still missing within 25 pc, particularly those with spectral types later than L8 and distances close to the 25 pc limit.

Key words. catalogs – stars: distances – Hertzsprung-Russell and C-M diagrams – stars: luminosity function, mass function – solar neighborhood – Galaxy: stellar content

1. Introduction

Hertzsprung (1922) was probably the first to notice that the systematic study of the stars in the solar neighbourhood is scientifically very valuable, for a multitude of reasons. First and foremost, the solar neighbourhood stars are the brightest (in terms of apparent magnitude) and largest (in terms of angular size) representatives of each spectral type, which allows us to observe them more easily, while they can serve as proxies for more distant stars of the same type. Furthermore, the stellar sample in the solar neighbourhood provides the most complete census of the Galactic disc population, covering more than 20 mag in absolute visual brightness.

Often, the solar neighbourhood stars are used to develop concepts that are later applied elsewhere in the universe. Applications span a diverse range of astronomical topics, such as the number of stars in the Galaxy and Galactic disc modelling (Pritchet 1983; Bahcall 1986; Binney 2010; Just & Jahreiß 2010), the present-day and the initial mass functions (Miller & Scalo 1979; Rana & Basu 1992; Sollima 2019), the stellar luminosity function and its fine structure (Reid et al. 2002; Chabrier 2003; Bahcall 1986; Upgren & Armandroff 1981; Wielen et al. 1983; Kroupa et al. 1990; Jao et al. 2018), constraints on star formation (Kirkpatrick et al. 2019), the local stellar surface density (McKee et al. 2015), stellar multiplicity (Duquennoy & Mayor 1991; Dieterich et al. 2012), brown dwarfs (Meisner et al. 2020), and target lists for exoplanet searches (Reiners et al. 2018; Turnbull & Tarter 2003). This compilation is certainly not exhaustive; the cited works merely serve as an illustration of studies that have been conducted in each field. The solar neighbourhood sample thereby often complements other large photometric and spectroscopic datasets that have become available, such as RAVE (Steinmetz et al. 2020), SDSS (Ahn et al. 2020), and PanSTARRS (Kaiser et al. 2002).

The number of surveys that are based on the nearby stars sample is expected to grow considerably in the future, especially due to the many endeavours to discover and characterise exoplanets. NASA has acknowledged the fact that many of the upcoming exoplanet search programmes overlap in their target lists, especially for the nearby stars, and has established a working group (SAG 22) on the topic of a target star archive (Hinkel et al. 2021). Nearby stars possess several advantages over more distant stars as exoplanet hosts, such as better resolution for direct imaging
(HabEx, Gaudi et al. 2020; LUVOIR, The LUVOIR Team 2019) or better stellar characterisation. Continued interest in the nearby stars sample is thus expected for the foreseeable future.

For these reasons, we present here an update of the Catalogue of Nearby Stars, denoted CNS5. An update was indeed due as since the publication of the Preliminary Version of the Third Catalogue of Nearby Stars (Gliese & Jahreiß 1991), a fourth version of the catalogue, CNS4, was prepared by Hartmut Jahreiß but never published. While the CNS4 was, for the most part, based on space-based parallaxes from HIPPARCOS (ESA 1997; van Leeuwen 2007a, b), the CNS5 incorporates Gaia data (from the release Gaia EDR3, Gaia Collaboration 2021a; Lindegren et al. 2021b). Due to Gaia’s superb astrometric precision and its large number of catalogue sources down to $G \sim 20$ mag and fainter, the completeness of the nearby star sample and the accuracy of astrometric and photometric parameters are greatly improved. At the same time, the number of falsely included stars is also dramatically reduced.

As opposed to the recently published Gaia Catalogue of Nearby Stars (GCNS, Gaia Collaboration 2021b), which lists all stars within 100 pc, the CNS5 adheres to its traditional volume of 25 pc around the Sun. The CNS5 is not based purely on Gaia data, but also incorporates data from HIPPARCOS where favourable, as well as from the CNS4 and from ground-based astrometric surveys carried out in the near-infrared. It aims for completeness and cleanliness of the final nearby stars sample to the extent possible, in order to facilitate statistical studies based on the volume-limited sample as a whole. In contrast, the GCNS includes all stars with a non-zero probability of lying within 100 pc, so it is aimed more at completeness rather than cleanliness near the distance limit. Naturally, completeness is higher in the CNS5 compared to the GCNS, but this comes at the expense of a smaller volume. The applications of the two catalogues are thus to some extent complementary.

The compilation of the CNS5 is much more complicated than just selecting all sources with parallaxes larger than 40 mas. The reasons include a number of issues: (i) spurious catalogue entries with apparently large parallaxes (Lindegren et al. 2021b; Gaia Collaboration 2021b), which have to be filtered out; (ii) blended sources whose photometry has to be deblended so that they can be reliably placed into a Hertzsprung-Russell diagram; and (iii) the various components of multiple systems that have to be treated in a consistent way, even if reliable parallaxes do not exist for all of the components. Furthermore, we do not only use Gaia EDR3, but also the HIPPARCOS Catalogue (ESA 1997) for the brighter stars missing in Gaia as well as ground-based infrared parallax surveys (Best et al. 2021; Kirkpatrick et al. 2021) for the red and optically faint objects such as brown dwarfs. We also derive completeness limits and white dwarf (WD) and main-sequence star luminosity functions.

The paper is organised as follows. In Sect. 2, we describe various other catalogues of nearby stars, both previous and current. In Sect. 3, we present the philosophy behind the compilation of the CNS5 as well as our methods. Section 4 provides a description of the catalogue content, while Sect. 5 addresses completeness limits as well as the luminosity function; it also presents the colour-magnitude diagram (CMD) of all catalogue stars. Section 6 features our conclusions and a summary. Detailed descriptions of algorithms are provided in the appendices.

2. Overview of the catalogues of nearby stars

2.1. Catalogue of Nearby Stars series (CNS)

2.1.1. Previous editions

The first version of the Catalogue of Nearby Stars (CNS1) was published by Gliese (1957); it contained 1094 stars (915 systems) within 20 pc. The subsequent update of the catalogue (CNS2) expanded the coverage to 22.2 pc and contained 1627 stars in 1313 systems (Gliese 1969). It lists photometric, spectroscopic, and trigonometric parallaxes as well as the ‘resulting parallax’, an estimate of the best value considering all measurements.

The CNS3, entitled Preliminary Version of the Third Catalogue of Nearby Stars, lists 3403 stars within the 25 pc distance limit (Gliese & Jahreiß 1991). In contrast to the CNS2, the resulting parallax in the CNS3 is the trigonometric parallax, unless it is either not available or has unusually large errors. Although this version of the catalogue was denoted as ‘preliminary’, it is still the most recent publicly available edition of the CNS (a ‘final’ version was never published). Therefore, many recent publications are still based on the CNS3 (e.g. Tamazian & Malkov 2014; Bar et al. 2017; Price et al. 2020 to name a few).

The fourth version (CNS4) was created by Jahreiß & Wielen (1997). It contained ground-based parallaxes as well as trigonometric parallaxes from HIPPARCOS. However, the data from previous versions of the CNS series was not fully homogenised with the new data, which leads to inconsistencies.

Over the decades, one of us (Hartmut Jahreiß) has continuously scanned the literature to update astrometry, photometry, and other supplementary data (radial velocities, binary information) of potential nearby stars. This information has also been used in the construction of the CNS5.

2.1.2. Numbering scheme in the CNS

Stars in the CNS1 were designated as $G \, \text{NNN}$, where $\text{NNN}$ represents the consecutive integer number ordered by right ascension. In the CNS2, designations were formatted as $G \, \text{NNN}.x$, adding a decimal place for the new stars. This allowed the original Gliese star numbers to be preserved and the ordering system by right ascension to be kept.

Since the publication of an extension to CNS2 (Gliese & Jahreiß 1979), the stars were referred to as $G \, \text{NNNN}$. In addition, the CNS3 listed Woolley numbers (Woolley et al. 1970) and introduced NN designations for new stars; both of them have been replaced with Gliese-Jahreiß (GJ) numbers in the meantime. By now, all the previously known nearby stars thus have GJ designations. One can still tell from where they originated by their number; Woolley numbers start at 9001, and the largest assigned number is 9850, while NN numbers range from 3001 to 4388. The widely used GJ numbers have been kept in the CNS5 (see Sect. 4.1 for details).

2.2. Other catalogues

2.2.1. The RECONS project

The REsearch Consortium On Nearby Stars (RECONS; founded in 1994) has made an enormous effort to discover and characterise stars and ultra-cool dwarfs in the 25 pc volume, primarily by measuring their trigonometric parallaxes from the ground (e.g. Henry et al. 2018). They provided updated astrometric, photometric, and multiplicity information, and identified many
new nearby stars since the publication of the Yale Parallax Catalog (van Altena et al. 1995). Their results are published in The Solar Neighborhood series of papers in The Astronomical Journal (49 papers as of June 2022), making the compilation of the 25 pc sample from their work rather cumbersome. Only statistics for the 10 pc volume are given on their website. As of 2018, the RECONS database contained 317 systems within 10 pc. An overview of new nearby stars within 10 pc discovered by RECONS is provided in Henry et al. (2018).

2.2.2. Catalogue of stars within 50 pc based on Gaia DR2

Torres et al. (2019) studied the dynamical evolution of the comets in the Oort cloud. In particular, they characterised stellar encounters with the Solar System by integrating their orbits based on Gaia DR2 data. For this purpose, the catalogue of stars within 50 pc based on Gaia DR2 data has been constructed. The catalogue lists 14 659 stars. However, the approach used for source selection is a potential concern. Sources with high-quality astrometry were selected based on the relative uncertainty of the parallax (smaller than 20%), flux excess factor, and unit weight error (UWE). The re-normalisation of the UWE (RUWE; Lindegren 2018) was not incorporated when selecting sources for the catalogue. Such re-normalisation would preserve objects with extreme colours (e.g. such as brown dwarfs) from being removed because, contrary to the UWE, not only is the object’s G magnitude taken into account when calculating the RUWE, but its colour is too.

As the authors pointed out themselves, the catalogue is incomplete. The prime culprit here is the Gaia magnitude limit and, as a consequence, a significant number of faint low-mass stars are not detected. Furthermore, some of the brightest sources are also missing due to the Gaia saturation limit.

2.2.3. GCNS

The GCNS (Gaia Collaboration 2021b) aims to identify all sources in Gaia EDR3 with reliable astrometry and a non-zero probability of being located within 100 pc of the Sun. This is done by retrieval of sources with parallaxes larger than 8 mas, removal of spurious sources with machine-learning (using the random forest classifier) and by Bayesian distance estimation for the remaining sources.

The full catalogue lists 331 312 sources. The overall completeness of the GCNS is expected to be 95% or better for spectral types up to M8 (translating into $M_G = 15.7$ mag).

It is important to bear in mind that the prime focus of the GCNS is to provide a homogeneous census of nearby stars. Its volume is larger than that of the CNS5, but bright and red sources could be missing since the GCNS is based only on Gaia EDR3 data. As we will see, due to the inclusion of infrared surveys in the CNS5, the CNS5 is complete for much later spectral types well into the brown dwarf regime.

2.2.4. The 10 pc sample by Reylé et al. (2021)

Reylé et al. (2021) compiled the sample of stars, brown dwarfs, and exoplanets located within 10 pc of the Sun as a quality assurance test for the GCNS. Using this sample, it is possible to not only identify very nearby stars that are missing from the GCNS (or future Gaia data releases), but also to infer the level of completeness of the GCNS by estimating the expected number of objects of different types from the number densities for the 10 pc volume.

Objects for the 10 pc sample were selected from SIMBAD using a strict cut on parallax $\geq 100$ mas, with parallax uncertainties playing no role in the selection process. The sample was supplemented with components of unresolved binaries, brown dwarfs with recently published parallaxes from Best et al. (2021) and Kirkpatrick et al. (2019, 2021), and confirmed exoplanets from the Extrasolar Planets Encyclopædia1 as well as from the NASA Exoplanet Archive2.

The sample consists of 540 objects (including 77 exoplanets) in 339 systems. The Sun and its planets are not included. The 10 pc sample has separate entries for every object, including the unresolved components of multiple systems and exoplanets.

Naturally, among the catalogues reviewed in this section, the 10 pc sample by Reylé et al. (2021) has the highest level of completeness due to its smaller volume. At the same time, the number of objects contained within this volume is insufficient for statistical studies of the solar neighbourhood.

Future updates of the 10 pc sample are anticipated to have only a minor impact on the stellar content of the sample; the majority of the new additions to the sample are expected to come from single stars that have been resolved into multiple components. In the sub-stellar regime, the expected additions will be ultra-cool dwarfs (particularly those in the Galactic plane) and, of course, new exoplanets.

3. Construction of the CNS5 catalogue

3.1. Data selection

Our goal for the compilation of the CNS5 is to maximise completeness within the 25 pc limit. Therefore, the wealth of data from several different catalogues and surveys has to be carefully selected and combined. In the following subsections, we give a full account of our selection criteria, applied corrections, and how we combined data from the different catalogues to consolidate the CNS5.

3.1.1. Gaia EDR3

Due to its high levels of completeness and accuracy, Gaia EDR3 is an excellent starting point for the preparation of a catalogue of nearby stars. For the vast majority of objects, the Gaia parallax clearly indicates whether the star is located within 25 pc of the Sun or not. Therefore, the CNS5 is built primarily based on the data selected from Gaia EDR3 and then, if necessary, supplemented with data from HIPPARCOS and other catalogues and sources.

The primary sample for the CNS5 is constructed by retrieving all the objects that are possibly located within 25 pc of the Sun from Gaia EDR3:

$$\sigma_{\text{EDR3}} Z_{5.6} > 40 \text{mas},$$

where $\sigma_{\text{EDR3}}$ denotes the measured parallax in the Gaia EDR3 catalogue, $Z_{5.6}$ its standard error, $Z_{5.6}$ is the parallax zero point for the five- and six-parameter solutions in Gaia EDR3, and $\eta$ is the parallax error inflation factor. The parallax zero-point correction and the inflation factor for the parallax error are discussed below. The query returns 5876 sources.

Sources with spurious astrometric solutions are removed by applying a simple yet powerful cut on the amplitude of the Image Parameter Determination goodness-of-fit (IPD GoF):

1. https://exoplanet.eu/
2. https://exoplanetarchive.ipac.caltech.edu/
clear whether these objects even belong to the 25 pc volume. Thus, it is not

astrometric solution (which is based on the assumption of the

we do not know the true parallaxes of these objects since their

comes down to the 12 objects listed in Table A.1. Furthermore, the number of rejected objects should be negligible and probably
down to the 12 objects listed in Table A.1. Furthermore, we do not know the true parallaxes of these objects since their

of Eq. (2), we avoid introducing a selection bias against, for

ruwe, where the re-normalisation factor is a function of the

is opposed to other widely used selection criteria such as the

RUWE can be induced not only by the binarity of an object, but

RUWE, where the re-normalisation factor is a function of the

parameters themselves are not involved in the selection process. This

ruwe, in addition to the photometric factors (Belokurov et al. 2020). Such

G-band magnitude and the

The parallaxes from

EDR3 temporal baseline. Over

EDR3 is based on data collected over 34 months

EDR2 is based on 22 months of observations,

this decision. Typically, the parallax uncertainties in

Gaia EDR3 are smaller by a factor of 0.8 or better than in

Gaia DR2 due to improved calibrations and the longer time span of the observations; Gaia DR2 is based on 22 months of observations, while

Gaia EDR3 is based on data collected over 34 months (Lindegren et al. 2021b). In a few cases, the opposite is true, and, despite the longer time span of the observations, the parallax uncertainty is larger in

Gaia EDR3. This can often be a consequence of the object being an unresolved binary with the orbital period comparable with the Gaia EDR3 temporal baseline. Over time, the contribution of the orbital motion accumulates and can induce a photocentre perturbation. This leads to the significant inconsistency of the observed displacement of the source with

3 In the form of an effective wave number, \( v_{\text{eff}} \), for a five-parameter solution, or a pseudo-colour, \( \nu_{\text{eff}} \), for a six-parameter solution.

4 https://www2.mpia-hd.mpg.de/homes/calj/gedr3_distances/FAQ.html
the single-star model fit, which in turn translates into increased uncertainties of parallaxes and proper motions.

Furthermore, we decided against adding new objects with the parallaxes from Gaia DR2, which have just two-parameter solutions in Gaia EDR3 or are missing completely. The vast majority of such sources have spurious solutions in Gaia DR2 and did not meet the acceptance criteria during reprocessing in Gaia EDR3 (Lindegren et al. 2021b). Including these sources would thus contaminate our catalogue. We would like to remark that sources with spurious solutions in Gaia DR2 cannot be eliminated with our criterion in Eq. (2) since the IPD GoF statistics are not included in that data release. Finally, it appears not to be feasible to construct a volume-limited sample of nearby stars based on Gaia DR2 that would be free from spurious entries and at the same time without removing too many real sources. As we outline above, the widely used selection criteria – namely RUWE and the photometric excess factor – are sub-optimal for this task. Alternatively, applying machine learning will not necessarily provide a classification that is robust enough. As reported in Gaia Collaboration (2021b), when the same random-forest classifier as that used to construct the GCNS has been applied to Gaia DR2 (but with the predictive variables adapted to those available in Gaia DR2), the resulting sample still contained 15 sources with \( \sigma > 500 \) mas, whereas in Gaia EDR3 there are only two such sources – Barnard’s star and Proxima Centauri.

3.1.2. HIPPARCOS

While Gaia EDR3 includes the majority of known nearby stars, it is certainly not complete, as the very brightest stars in particular are missing. As the next step, we thus supplemented our Gaia EDR3 sample with entries from the HIPPARCOS Catalogue (Perryman et al. 1997), which is complete for \( V \) magnitudes brighter than 7.3–9.0 mag. By doing so, we added objects that are too bright for Gaia and thus missing, or that do not have a full astrometric solution in Gaia EDR3. Furthermore, Gaia EDR3 is incomplete for high proper motion stars: \( \sim 8\% \) of known stars with proper motions \( \geq 0.6 \) arcsec yr\(^{-1} \) are missing from Gaia EDR3 (Fabricius et al. 2021). Another major advantage of including data from HIPPARCOS is that for very bright objects it usually provides astrometry of higher quality than the one from Gaia EDR3.

Similarly to the selection of stars from Gaia EDR3, objects from the HIPPARCOS Catalogue were selected based on their parallax. In addition, we impose an upper limit on parallax error to avoid adding objects with extremely large parallax uncertainties, which often result from a photocentre wobble of unresolved or marginally resolved binaries:

\[
\begin{align*}
(i) & \quad \sigma + 3\sigma \geq 40 \text{ mas} \\
(ii) & \quad \sigma \leq 10 \text{ mas}
\end{align*}
\]

where \( \sigma \) is the parallax from the HIPPARCOS Catalogue and \( \sigma \) its formal error. In this work, we used the second reduction of the HIPPARCOS astrometric catalogue with improved parallaxes and their formal errors (van Leeuwen 2007a,b). The selected sample contains 2007 sources. We adopted the cross-match with Gaia EDR3 provided by Marrese et al. (in prep.) and described in Marrese et al. (2021).

A comparison of parallax errors from HIPPARCOS and Gaia EDR3 shows that for objects fainter than \( G \approx 6 \) mag, the Gaia EDR3 parallaxes typically have a level of precision that is one-to-two orders of magnitude higher than those measured by HIPPARCOS. However, parallaxes from HIPPARCOS for very bright objects have smaller standard errors, due to the saturation limit of Gaia. Figure 2 shows the ratio of parallax errors from HIPPARCOS and inflated errors from Gaia EDR3 \( (\sigma_{\text{HIP}/\sigma_{\text{EDR3}}} \leq 1) \) as a function of the Gaia \( G \)-band magnitude. We find that for the objects brighter than \( G \approx 4 \) mag, HIPPARCOS parallaxes are typically better (i.e. \( \sigma_{\text{HIP}/\sigma_{\text{EDR3}}} < 1 \)). Therefore, the parallax values with the smaller uncertainties \( (\sigma_{\text{HIP}} \text{ or } \sigma_{\text{EDR3}}) \) will be adopted as a resulting parallax in the CNS5 for those objects which are present in both catalogues, Gaia EDR3 and HIPPARCOS.

3.1.3. Ultra-cool dwarfs

Objects fainter than the Gaia magnitude limit of 20–21 mag in the \( G \) band are so far missing from our sample. This concerns many of the L and T dwarfs in the 25 pc volume. Thus, we decided to add nearby ultra-cool dwarfs from the compilation by Best et al. (2021), who recently provided a sample that is complete within 25 pc for spectral types from L0 to T8. All stars in their sample have parallaxes, many of them measured as part of the Hawaii Infrared Parallax Program (Dupuy & Liu 2012, and later papers in the series). As the next step, we updated and supplemented the resulting sample with Spitzer parallaxes from Kirkpatrick et al. (2021).

As usual, we only included objects that are possibly within the 25 pc volume according to Eq. (3) and discarded objects with parallax errors larger than 10 mas. Again, only trigonometric parallaxes were considered. This resulted in a sample of 906 objects. Typical parallax errors in the resulting sample of ultra-cool dwarfs range from 1 to 10 mas, which is larger than those from HIPPARCOS and Gaia. Nevertheless, adding the ultra-cool dwarfs helps tremendously with completeness towards the smallest masses. In total, 462 ultra-cool dwarfs without counterparts in Gaia EDR3 were added to the CNS5 from the sample of Best et al. (2021), and 79 were taken from the sample of Kirkpatrick et al. (2021).

3.1.4. CNS4

We add sources from the internal version of the CNS4 which are missing so far in our sample from Gaia EDR3, HIPPARCOS
and Best et al. (2021). This is done by identifying and discarding those objects in CNS4 that (i) are already included in our sample; (ii) now have higher precision parallax measurements that move them outside the 25 pc limit; (iii) were classified as a nearby star in the past, whereas newer studies show that they actually have non-stellar nature such as, for instance, a plate flaw (GJ 2087) or even BL Lac objects (GJ 3750 and GJ 3848); (iv) are sources listed as a component of a nearby star, whereas newer studies could not confirm them, concluding that they are non-existing or showing that they are not physically bound and therefore are background stars; (v) have trigonometric parallaxes with errors exceeding an upper limit of 10 mas; (vi) only have the photometric parallax measured.

Cross-matching the CNS4 with our sample was often complicated by inconsistencies between listed designations and coordinates, which were not always up to date. Such cases had to be handled manually and frequently required significant amounts of detective work.

For every object retained in the resulting sample, we collected updated astrometry from the literature and supplemented it with optical, near-infrared (NIR), and mid-infrared (MIR) photometry whenever possible. Our attempts to identify a counterpart in Gaia EDR3 with a two-parameter solution were successful for objects predominantly of intermediate brightness, whereas an unambiguous identification of Gaia EDR3 counterparts for fainter objects was often stymied by the presence of two or more sources of similar brightness (and with only a two-parameter solution in Gaia EDR3 for them) in the vicinity. Confident cross-matching with Gaia EDR3, even when only a two parameter solution was available, provides not only highly accurate coordinates but also photometry in the Gaia bands. When combined with parallaxes from the literature, this allows us to reliably place these sources in the CMD.

The objects added from the CNS4 are typically M dwarfs of intermediate brightness with only a two-parameter solutions in Gaia EDR3. The additional 27 objects from CNS4 are crucial to maximise completeness of the CNS5.

3.2. The Sun

As pointed out in the introduction, the aim of the CNS5 is to provide the most complete census of nearby stars possible, so that it can be used for statistical studies of the solar neighbourhood. Thus, there is no real reason not to include the nearest star – the Sun. On the other hand, due to its proximity, its treatment is different from that of other stars in the catalogue, and a few notes have to be made here.

In the catalogue entry for the Sun we only list apparent magnitudes in different photometric bands. Consistently with previous versions of the CNS catalogues, we do not assign any GJ designation to this entry.

Traditionally, the distance between the Sun and Earth (and thus absolute magnitudes of the Sun) was estimated from the solar parallax\(^5\). The determination of the solar parallax has been a fundamental problem in observational astronomy over the centuries (Bond 1857; Tupman 1878; Hinks 1909; Turner 1912; Weaver 1943; Thomson et al. 1961). For an overview of principles of the determination of the solar parallax with Gaia, we refer the reader to Mignard (2020). However, since 2012 the astronomical unit (au) has been a conventional unit of length and equals exactly 149 597 870 700 m (translating to the solar parallax of \( \pi_0 = 8.794143836'' \)), as defined by IAU (2012). Given that the stellar parallax is non-definable for the Sun and that our catalogue only lists trigonometric stellar parallaxes, no parallax value is given for the Sun.

Turning now to photometry, the solar magnitudes and colours serve as an important reference point in many areas of astrophysics. However, we do not have a measured value of either \( G_0 \), or its colours (\( G − RP \)) or (\( BP − RP \)). The approach to be taken here is to use magnitudes and colours estimated from flux-calibrated solar reference spectra. Casagrande & VandenBerg (2018) reported magnitudes of the Sun in the Gaia bands in the Vegamag system derived from absolute flux measurements, both ground-based and from space, combined with model spectra. Hence, we adopted \( G_0 = -26.90 \) mag (this corresponds to an absolute magnitude of \( M_G = 4.67 \) mag), \( G − RP = 0.49 \) mag and \( BP − RP = 0.82 \) mag for the Sun.

Similarly, Willmer (2018) estimated the apparent and absolute magnitudes of the Sun in a large number of other broad-band filters used in various surveys and observatories. Thus, we tabulate the NIR and MIR magnitudes of the Sun in the CNS5, that is, in 2MASS, WISE, and the system derived from absolute flux measurements, both ground-based and from space, combined with model spectra. Hence, we adopted \( G_0 = -26.90 \) mag (this corresponds to an absolute magnitude of \( M_G = 4.67 \) mag), \( G − RP = 0.49 \) mag and \( BP − RP = 0.82 \) mag for the Sun.

4. Description of the catalogue

4.1. Numbering scheme

All objects in the catalogue are designated in the following format: CNS5 NNNN, where NNNN represents the sequence number assigned consecutively when entries are ordered by right ascension. This running number is unique for every object within the CNS5. Objects in the next releases of the catalogue will be renumbered entirely (with the corresponding acronym that specifies the release number: e.g. CNS6).

In addition, the widely used GJ numbers have been kept in the CNS5. 3 461 new objects in the catalogue were given GJ numbers for the first time. GJ numbers assigned in the CNS5 range from GJ 10001 to GJ 13461. Contrary to CNS5 numbers, GJ numbers are not ordered by right ascension and do not have to be unique for every object – different components of binary or multiple systems may have the same GJ number.

Frequently, information on the binarity of an object is encoded in a designation by appending the suffixes A, B, and so on to the system’s designation. This approach could be confusing and sometimes could even lead to erroneous notations in publications.

For example, Proxima Centauri (= GJ 551 = \( \alpha \) Cen C) is occasionally referred to as GJ 551 C. However, neither GJ 551 A nor GJ 551 B exist. \( \alpha \) Cen A and \( \alpha \) Cen B are GJ 559 A and GJ 559 B, respectively.

To avoid further confusion in cases when a primary and a secondary component have different designations or new information on binarity of an object has become available, we decided to keep indexing of binary and multiple systems in the CNS5 separately from the designations. This is done by introducing additional columns in the CNS5 where we list the GJ number for the system (gj_id), suffixes for a component (component_id), the total number of components in a system (n_components), and, if the GJ number for a component differs from the GJ number of the primary of the system, the GJ number of the primary (gj_system_primary). This is shown in Table 1 for the example of the triple system \( \alpha \) Cen. In cases where we assigned new

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\(^5\) Defined as the angle subtended by the equatorial radius of the Earth at the mean distance of the Sun.
GJ numbers to binary or multiple systems, we assigned separate GJ numbers for each component listed in the CNS5.

Components are designated in the CNS5 with capital letters in descending order of brightness in the GJ numbers for each component listed in the CNS5. We opted not to designate components in the order of their separation from the primary, as it is frequently done, since the separation, especially that of nearby multiple systems, is changing with time.

### 4.2. CNS5 content

The data structure of the CNS5 is described in detail in Table 2. Columns (1–4) contain object identifiers. In addition to CNS5 and GJ designations, we also provide, if available, object identifiers in the HIPPARCOS and Gaia EDR3 catalogues. This facilitates cross-matching of our catalogue with other catalogues by using one of these identifiers.

Positions in our catalogue are not propagated to the common reference epoch, but are provided at the mean epoch of the original catalogue. This implies that the epoch is not constant throughout the CNS5 catalogue. The epoch to which the position refers is listed for each object in the epoch column. References for coordinates, as well as for all other parameters listed in the CNS5, are provided in the form of bibliodes as assigned by the SAO/NASA Astrophysics Data System.

Parallaxes listed in the CNS5 are always trigonometric; no photometric or spectroscopic parallaxes were considered. Parallaxes, when selected from Gaia EDR3, are corrected for the parallax zero point, and the corresponding errors are the inflated ones. Proper motions for all stars are listed as well, and for all but 82 sources they come from the same reference as the parallax.

The G-band photometry of Gaia EDR3 sources with two-parameter or six-parameter astrometric solutions is corrected as described in Riello et al. (2021); Gaia Collaboration (2021a). Magnitudes in Gaia EDR3 are listed without uncertainties. The error values given in the CNS5 are calculated from the electron flux and its relative error as

$$\sigma_X = \frac{2.5}{\ln(10)} \sigma_{I_X},$$

where $X$ is the corresponding Gaia band (G, BP or RP) and $I_X$ is the flux in this band. For simplicity, we neglect the asymmetry of the error distribution for sources with a low flux-over-error ratio ($I/\sigma_I \lesssim 10$). The assumption of symmetric errors is reasonable; all sources with $G$ magnitudes in the CNS5 have $I_G/\sigma_{I_G} > 10$, and the sources with a low flux-over-error ratio in RP or BP bands represent a tiny minority in the CNS5 (13 sources with $I/\sigma_I < 10$ in RP band and 286 such sources in BP band).

For objects with photometry in Gaia EDR3 we also list the synthetic (deblended) $G$ and $G - RP$ magnitudes. These are calculated from our model fit to the Gaia data for a sample of objects with high-quality photometry and are fully described in Appendix B. The deblended magnitudes in our catalogue are only provided for sources with a sufficiently large flux-over-error ratio in $BP$ and $RP$ bands ($I_{BP,RP}/\sigma_{BP,RP} > 20$) and with a colour within the applicability range of $0 \text{ mag} < BP - RP < 4.25 \text{ mag}$.

We supply the deblended photometry for all sources that match these criteria, irrespective of whether the correction is significant. In case it is available, the deblended photometry is always given as the resulting photometry.

For all objects selected from the HIPPARCOS catalogue, which have no counterpart in Gaia EDR3, we provide converted values of $G$ and $RP$ magnitudes. Converted magnitudes were calculated using the photometric relationships $G = H_p = f(V - I)$ from Riello et al. (2021). We opted for this parameter space because here, contrary to $(G - H_p, B - V)$, red giants and dwarfs display the same behaviour and no distinction between them is needed. However, the reader should be aware that $V - I$ colours in HIPPARCOS are a compilation from the literature and originate from a variety of ground-based measurements obtained more than 30 yr ago. As demonstrated by Koen et al. (2002) and by Platais et al. (2003), $V - I$ colours listed in HIPPARCOS in some cases can be grossly incorrect and should be treated with caution.

The remaining columns referring to photometry contain NIR and MIR magnitudes in the 2MASS ($J, H$ and $K_s$) and WISE ($W1, W2, W3$ and $W4$) passbands with their corresponding uncertainties. We used the cross-match between Gaia and 2MASS and Gaia and WISE, respectively, provided with Gaia EDR3, for the identification of objects. The photometric content of the CNS5 is summarised in Table 3.

Furthermore, we list the number of components in each system in the CNS5. We made an effort to identify at least obvious common proper motion pairs in the CNS5 by selecting pairs with projected separation less than 1 pc and proper motions consistent with a Keplerian orbit (see El-Badry et al. 2021, Eqs. (1) and (3)–(6) in their paper).

The limit on the projected separation of 1 pc corresponds to the separation where the Galactic tidal field typically starts to dominate the gravitational attraction of two stars (e.g. Binney & Tremaine 2008; El-Badry et al. 2021). The chosen limit seems to be appropriate since we found no pairs with a projected separation above 0.85 pc, and only two pairs (0.3%) with a projected separation larger than 0.33 pc. All separations are thus well below the adopted limit, so these systems have a high probability of being physically associated. The mean projected separation of the identified common proper motion pairs is 1857 AU, whereas the median is 185 AU (corresponding to an orbital period of $\sim 80,000$ and $\sim 2500$ yr, respectively, for a typical binary with a total mass of $1 M_\odot$).

We consider a pair of stars to be a common proper motion pair if its observed scalar proper motion difference does not exceed the maximum expected proper motion difference for a circular orbit of a binary with a total mass of $5 M_\odot$ at the $2\sigma$ level. For 86.6% of the identified pairs, we found that the observed proper motion difference is at least two times smaller than the expected difference due to orbital motion. Only 0.6% (four pairs) have a proper motion difference larger than the

| cns5_id  | gj_id | component_id | n_components | gj_system_primary |
|---------|-------|--------------|--------------|------------------|
| CNS5 3591 | 551   | C            | 3            | 559              |
| CNS5 3627 | 559   | AB           | 3            | –                |
Table 2. Description of CNS5 content.

| Column name          | Unit         | Description                                                                 | Example                  |
|----------------------|--------------|----------------------------------------------------------------------------|--------------------------|
| cns5_id              |              | CNS5 designation                                                           | 3591                     |
| gj_id                |              | Gliese-Jahreß number                                                       | 551                      |
| component_id         |              | Suffix for a component of a binary or multiple system                      | C                        |
| n_components         |              | Total number of components in the system                                   | 3                        |
| primary_flag         |              | Flag indicating the primary of a multiple system                           | False                    |
| gj_system primary    |              | GJ number of the primary component of the system                           | 559                      |
| gaia_edr3_id         |              | Source identifier in Gaia EDR3                                            | 5853498713190525696      |
| hip_id               |              | HIPPARCOS identifier                                                      | 70890                    |
| ra                   | deg          | Right ascension                                                           | 217.39232147200883       |
| dec                  | deg          | Declination                                                               | -62.67607511676666       |
| epoch                | a            | Reference epoch for coordinates                                           | 2016.0                   |
| coordinates_bibcode  |              | Reference for ra, dec                                                     | 2020yCat.1350....0G      |
| parallax             | mas          | Absolute trigonometric parallax                                           | 768.0665391873573        |
| parallax_error       | mas          | Error of parallax                                                         | 0.056201234              |
| parallax_bibcode     |              | Reference for parallax                                                    | 2020yCat.1350....0G      |
| pmra                 | mas a⁻¹      | Proper motion in right ascension \((d(\alpha \cos \delta)/dt)\)             | -378.741008265163        |
| pmra_error           | mas a⁻¹      | Error of \(r\)                                                           | 0.0313860740422222       |
| pmdec                | mas a⁻¹      | Proper motion in declination                                              | 769.4650146478623        |
| pmdec_error          | mas a⁻¹      | Error of \(\delta\)                                                      | 0.05052453279495239      |
| pm_bibcode           |              | Reference for proper motion                                               | 2020yCat.1350....0G      |
| rv                   | km s⁻¹       | Radial velocity (spectroscopic)                                           | -22.4                    |
| rv_error             | km s⁻¹       | Error of \(r\)                                                           | 0.5                      |
| rv_bibcode           |              | Reference for the radial velocity                                         | 2006A&A...460..695T      |
| g_mag                | mag          | \(G\) band mean magnitude (corrected)                                      | 8.984749                 |
| g_mag_error          | mag          | Error of \(g\)                                                           | 0.0007106                |
| bp_mag               | mag          | \(Gaia\) EDR3 integrated \(BP\) mean-magnitude                           | 11.373116                |
| bp_mag_error         | mag          | Error of \(bp\)                                                          | 0.00025825               |
| rp_mag               | mag          | \(Gaia\) EDR3 integrated \(RP\) mean-magnitude                           | 7.5685353                |
| rp_mag_error         | mag          | Error of \(rp\)                                                          | 0.0017553                |
| g_mag_from_hip       | mag          | Converted \(G\) band magnitude from HIPPARCOS                             |                          |
| g_mag_from_hip_error | mag          | Error of \(g_{mag}\) from \(hip\)                                        |                          |
| g_rp_from_hip        | mag          | Converted \(G - RP\) colour from HIPPARCOS                               |                          |
| g_rp_from_hip_error  | mag          | Error of \(g_{rp}\) from \(hip\)                                        |                          |
| g_mag_resulting      | mag          | Resulting \(G - \) band magnitude                                        | 8.984749                 |
| g_mag_resulting_error| mag          | Error of \(g_{mag}\) resulting                                           | 0.0007106                |
| g_rp_resulting       | mag          | Resulting \(G - RP\) colour                                              | 1.3984906                |
| g_rp_resulting_error | mag          | Error of \(g_{rp}\) resulting                                           | 0.0033824                |
| g_rp_resulting_flag  |              | Flag related to \(g_{rp}\) resulting                                      | 0                        |
| j_mag                | mag          | 2MASS \(J\) - band magnitude                                             | 5.357                    |
| j_mag_error          | mag          | Error of \(j\)                                                           | 0.023                    |
| h_mag                | mag          | 2MASS \(H\) - band magnitude                                             | 4.835                    |
| h_mag_error          | mag          | Error of \(h\)                                                           | 0.057                    |
| k_mag                | mag          | 2MASS \(K_s\) - band magnitude                                           | 4.384                    |
| k_mag_error          | mag          | Error of \(k\)                                                           | 0.033                    |
| jhk_mag_bibcode      |              | Reference for NIR magnitudes                                              | 2003tmc..book.....C      |
| w1_mag               | mag          | WISE W1 - band magnitude                                                  | 4.195                    |
| w1_mag_error         | mag          | Error of \(w1\)                                                         | 0.086                    |
| w2_mag               | mag          | WISE W2 - band magnitude                                                  | 3.571                    |
| w2_mag_error         | mag          | Error of \(w2\)                                                         | 0.031                    |
| w3_mag               | mag          | WISE W3 - band magnitude                                                  | 3.826                    |
| w3_mag_error         | mag          | Error of \(w3\)                                                         | 0.015                    |
| w4_mag               | mag          | WISE W4 - band magnitude                                                  | 3.664                    |
| w4_mag_error         | mag          | Error of \(w4\)                                                         | 0.024                    |
| wise_mag_bibcode     |              | Reference for MIR magnitudes                                              | 2014yCat.2328....0C      |

Notes. The entry for Proxima Centauri (GJ 551) is shown as an example. (a) The definitions of the flag values are as follows: 0 = resulting \(G - RP\) is deblended, 1 = resulting \(G - RP\) is uncorrected (i.e. \(Gaia\) EDR3 catalogue value is listed), 2 = \(G - RP\) is converted from HIPPARCOS.
Table 3. Description of the photometric content of the CNS5.

| Parameter                  | # of objects |
|----------------------------|--------------|
| g_mag                      | 5234         |
| bp_mag                     | 5148         |
| rp_mag                     | 5157         |
| g_mag_from_hip             | 137          |
| g_rp_from_hip              | 137          |
| g_mag_resulting            | 5372         |
| g_rp_resulting             | 5261         |
| j_mag                      | 5348         |
| h_mag                      | 5347         |
| k_mag                      | 5334         |
| w1_mag                     | 4812         |
| w2_mag                     | 4814         |
| w3_mag                     | 4812         |
| w4_mag                     | 877          |
| Has k_mag but no g_mag_resulting | 334    |
| Has g_mag_resulting but no k_mag | 372     |
| Has w1_mag but no g_mag_resulting | 537    |
| Has g_mag_resulting but no w1_mag | 1097   |

expected difference due to orbital motion but still consistent at the $2\sigma$ level with a Keplerian orbit. Loosening this selection criterion further would result in contamination from chance alignments with background stars.

When it comes to identifying common proper motion pairs in the CNS5, we decided to neglect the parallax discrepancy. This way we can also include nearby systems whose physical separation between components is large enough that their parallaxes differ significantly. This choice is justified by the low projected source density in the CNS5 catalogue and large parallaxes and proper motions of objects in the solar neighbourhood. We found that parallax discrepancy, $\Delta \varpi/\sigma_{\varpi} = |\varpi_1 - \varpi_2| / \sqrt{\sigma_{\varpi_1}^2 + \sigma_{\varpi_2}^2}$, for nearby binaries in Gaia EDR3 could be as large as 11.9$\sigma_{\varpi}$ (Gaia EDR3 5479222240596469632 and Gaia EDR3 5287046368477870848).

Finally, we would like to remark that the common proper motion pairs identified in the CNS5, by construction, include all the nearby binaries from El-Badry et al. (2021) as well as systems with three or more components and pairs where only one component has parallax and proper motion given in Gaia EDR3 and the second has them from other surveys, for instance from Spitzer. This results in 696 common proper motion pairs in the CNS5.

So far, we only consider visual binary or multiple components for the number of components given in the catalogue. Spectroscopic companions or otherwise detected companions from the literature will be added in the next version of the CNS catalogue. Finally, we provide radial velocities from Gaia EDR3 or from the compilations by Best et al. (2021) where available.

4.3. Availability of the CNS5 catalogue

The CNS5 catalogue is hosted by the German Astrophysical Virtual Observatory (GA VO) and is also available through the VizieR Catalogue Service.

5. Catalogue properties

5.1. Colour-magnitude diagrams

Figure 3 (top) shows the CMD for the selection of Gaia EDR3 objects in the CNS5 with published (i.e. unadjusted) colours. Here, we see that some objects have a large offset towards the red of the main sequence, which is unphysical and is caused by blending or contamination from nearby sources.

In order to correct for it, we derive synthetic $G - RP$ magnitudes (see Appendix B for details) in the applicability range of $0 \text{ mag} < BP - RP < 4.25 \text{ mag}$ and if the flux over error is greater than 20 for both $BP$ and $RP$ magnitudes. Figure 3 (bottom) shows the CMD using these synthetic $G - RP$ magnitudes for all stars, although the corrections are small for many of them (coded in blue in the figure). The stars coded in red have large corrections, and they now all fall right on the main sequence where one would expect them, illustrating that our correction works extremely well.

In Fig. 4 we show the infrared CMDs using 2MASS (top) and WISE (bottom) photometry. In both diagrams the blue points are sources with a counterpart in Gaia EDR3, while the objects in orange are absent in Gaia EDR3. In the 2MASS CMD, the lowest mass objects turn left towards the blue. This effect is associated with the 1.6 and 2.2 $\mu$m methane absorption.
bands (Burgasser et al. 1999) and with the dissipation of clouds across the L/T transition of brown dwarfs (Saumon & Marley 2008). As the absorption in cooler T dwarfs gets stronger, making their \( J - K_s \) colour bluer, these low-mass brown dwarfs approach the location of the WDs in the CMD. In contrast, in WISE \( W1 - W2 \) the ultra-cool dwarfs continue the trend towards the red for lower masses. As a result, the lower end of the main sequence in WISE is well separated from the WDs. Photometric errors for the fainter objects in particular are also smaller in WISE, and as seen in Sect. 4.2, WISE goes deeper and is more complete for ultra-cool dwarfs than 2MASS, thus making WISE ideal to study the faint end of the main sequence.

In Fig. 5, we present the CMD of the CNS5 objects in Gaia EDR3 and WISE bands combined. We used synthetic Gaia colours (Appendix B) where applicable and converted the magnitudes and colours of HIPPARCOS stars into the Gaia system to also include those stars in the plot. There are still a few stars located redwards of the main sequence; these are all stars for which we could not provide deblended magnitudes, either because they fall outside of the colour range where a reliable correction could be derived or they have the signal-to-noise ratio (S/N) smaller than 20. Their colours in the CMD are still dominated by blending or contamination, whereas their \( G \)-band absolute magnitude is reliable. We note that for objects in our catalogue the uncertainty of position in the CMD is dominated by colour uncertainty and not by that of the parallax. The mode of the underlying parallax error distribution in the CNS5 is 0.025 mas (see Fig. 6). This means that the parallax uncertainty typically contributes only about 0.0014 mas to the uncertainty of the absolute magnitude for an object at the 25 pc distance, whereas the mode of the \( G - RP \) uncertainty distribution is 0.0018 mag. From Fig. 4 (bottom), we know that the number of the main-sequence objects that do not have a counterpart in Gaia EDR3 starts to increase from \( M_{W1} \gtrsim 9 \) mag or \( M_0 \gtrsim 14 \) mag (see Fig. 9). This region is indicated by the grey shaded area in the main plot. We show this lower main-sequence region as an inset plot in the WISE bands, where the level of completeness is much higher than in Gaia.

### 5.2. Completeness of the CNS5

A precise assessment of the completeness of the CNS5 catalogue is essential not only to know until which absolute magnitude or spectral type we are complete, but it is also a crucial component for deriving a luminosity function (see Sect. 5.3) and for many other similar applications. Using a number density simply computed for the volume with a 25 pc radius would yield a luminosity function that is heavily biased due to incompleteness at the faint end. Consequently, number densities at faint magnitudes would be underestimated. In contrast, when number densities are derived within the completeness limit, this bias is avoided.

Assuming that stars in the solar neighbourhood have a constant number density, we define the completeness limit of the CNS5 as the largest distance, \( r_c \), at which the distribution of objects in the catalogue is still consistent with being spatially uniform. Beyond this distance, the observed number density starts to drop because more and more objects are too faint to be observed (or to have reliable parallaxes), and hence are missed in our volume-limited sample. Furthermore, it is natural to expect this distance, \( r_c \), to be smaller for objects with fainter absolute magnitudes.

A uniform space density prior is also reasonable for our 25 pc sample because there are no known clusters within this distance. The nearest cluster, the Hyades, is located at a distance of \( 47.50 \pm 0.15 \) pc from the Sun (Gaia Collaboration 2018) and has a half-mass radius of 4.1 pc and tidal radius of 9 pc (Röser et al. 2011). Using Gaia DR2, the present-day tidal tails of the Hyades were mapped within 200 pc of the Sun, and there are only 18 probable members and three contaminants located within 25 pc of the Sun (Röser et al. 2019). According to Jerabkova et al. (2021), the number of candidate members of the Hyades tidal tails located within 25 pc is even lower: they confirm only seven members using Gaia DR2 and five members when using more precise astrometry from Gaia EDR3 in their analysis. These numbers are not large enough to yield any statistically significant overdensity within our 25 pc volume or to contaminate the luminosity function of the solar neighbourhood.

We assessed the completeness of our catalogue using a Kolmogorov-Smirnov test. Here, we select a sub-sample of stars for each absolute magnitude bin for which a completeness limit should be estimated. Then, for each such sub-sample the cumulative distribution function (CDF) of the distance, \( r \), is derived and compared with the expected CDF of a uniform distribution.
Fig. 5. CMD of CNS5 objects in Gaia EDR3 and WISE bands. The main plot includes Gaia EDR3 objects with resulting $G - RP$ colours. This includes objects with synthetic colours and also objects that fall out of its applicability range. It also includes objects from HIPPARCOS that do not have a counterpart in Gaia EDR3, with converted $G$ and $RP$ magnitudes. The top and right axes show the spectral type and the blue cross represents the Sun’s location on this CMD. The grey shaded area corresponds to the region in which the number of main-sequence objects not present in Gaia start to increase in WISE bands. Thus, this region is also represented as an inset plot in WISE bands with the spectral type on the top axis. The colour bar shows the density in terms of star counts per pixel. On the main plot, each pixel is $[0.020 \times 0.15]$ mag while on the inset plot it is $[0.045 \times 0.25]$ mag$^2$. One extreme outlier falls outside of the main plot region.

Fig. 6. Parallax uncertainties in CNS5. The inset shows a zoomed-in view of the vertical axis and logarithmic scale being used on each of the axes. Distributions of the parallax uncertainties in the sub-samples from Gaia; HIPPARCOS and other references are overplotted separately.

A note should be made here that we do this on the component level and not on the system level. For simplicity, stars with distances close to the 25 pc limit were treated according to their nominal parallax values.

By applying the Kolmogorov-Smirnov test, we find the largest distance $r_*$ within 25 pc at which both the empirical and the uniform CDF are statistically indistinguishable at the 5% level. Within the derived distance, $r_*$, our catalogue can be regarded as statistically complete for the probed magnitude interval.

Here, we recall that the analytical CDF of the cumulative number of stars as a function of distance $n(r)$ for a sphere of radius $R_0 = 25$ pc, and uniform space density can be derived from the normalised probability density function (PDF):

$$n(r) = \frac{3 r^2}{R_0^3}. \quad (5)$$

Thus, the CDF of $n(r)$ is given as

$$CDF(r) = \frac{r^3}{R_0^3}, \quad 0 \leq r \leq R_0. \quad (6)$$

For each empirical sample, we constructed a corresponding test sample of $10^4$ objects. The distance of an object in the test sample is given by

$$r = R_0 \cdot y^{1/3}, \quad (7)$$

where $y$ is a random number between zero and one.

Figure 7 exemplifies CDFs and results of the Kolmogorov-Smirnov test for two cases. While the distribution of the sources in the magnitude bin centred at $G = 11.5$ mag (upper row) is consistent with being uniform over all probed distances up to 25 pc, it is evident that the empirical and analytical CDFs of the sources in the bin at $G = 20$ mag are considerably different (lower left panel) and the sample is statistically complete only up to 16 pc (lower right panel). For illustrative purposes,
Fig. 7. We illustrate how we estimate the completeness limit with the help of the Kolmogorov-Smirnov test. **Left column**: empirical (shown in blue) and analytical (shown in orange) CDFs. **Right column**: p value from the Kolmogorov-Smirnov test as a function of probed distance limit. The dashed line indicates the $p = 0.05$ threshold. Values below the threshold indicate that the empirical and analytical CDFs are significantly different, which means that the spatial distribution of objects in the subsample is not uniform anymore. Thus, the subsample cannot be regarded as statistically complete beyond the completeness radius. Two magnitude ranges are shown here as an example. The dashed line in the **lower left panel** denotes the re-normalised CDF using the derived completeness limit for this magnitude bin.

Fig. 8. Completeness limit as a function of absolute magnitude. **Left**: completeness limit in the $G$ band. The limit is computed for a sliding bin with a 0.1 mag step and 1 mag bin width. **Right**: completeness limit as a function of absolute magnitude in the $W_1$ band. Here, a 0.15 mag step and a 2 mag bin width was used. The completeness limits are 18.9 mag in the $G$-band and 11.8 mag in $W_1$.

we show that the empirical CDF is represented by the analytical CDF quite well when the latter is normalised at the derived completeness limit (dashed line in the lower left panel). Following the approach outlined above, we derive a completeness limit of 18.9 mag in $G$-band and of 11.8 mag in $W_1$-band absolute magnitudes (Fig. 8).

When comparing the completeness limits or the luminosity functions in optical and MIR wavelengths, an approximate relation between the absolute magnitudes in these wavelengths is useful. In order to derive the transformation coefficients, we used the sample of the main-sequence stars from the GCNS with counterparts in the CATWISE catalogue (Eisenhardt et al. 2020) in order to make the sample larger but comparable to the CNS5.

We used the following criteria:

(i) $M_G > 13.0$ mag
(ii) gcns_prob > 0.99
(iii) wd_prob < 0.05
(iv) Eq. (2): $A_{\text{GoF}} < 10^{-12} (\sigma/\bar{\sigma})^{2.61}$

The resulting sample contains 31 875 sources.

An approximate transformation between $M_{W_1}$ and $M_G$ magnitudes can be obtained with a cubic polynomial fit in this sample, for which we obtain

$$M_{W_1} = 0.0073714 M_G^3 - 0.3474 M_G^2 + 5.896 M_G - 25.6,$$  \hspace{1cm} (9)
where all absolute magnitudes are in units of ‘mag’. The resulting relation for the main-sequence stars fainter than $M_G = 13.0$ mag is shown in Fig. 9.

Applying this transformation to sources without a counterpart in Gaia EDR3 but with $W_1$ magnitudes, so that we obtain approximate $G$ magnitudes for those ultra-cool dwarfs as well, we estimate that the CNS5 is complete down to $G \approx 19.7$ mag (Fig. 10), 0.8 mag fainter than based on Gaia sources alone.

Given that WDs are quite rare and, as shown later, represent only 5% of the stellar content in the solar neighbourhood, we separately assessed the WD completeness. We selected objects located in the WD region of the CMD by defining the following cut (see Fig. 11):

(i) $M_G > 10.0$ mag $+ 5(G - RP)$
(ii) $G - RP < 1.0$ mag

Having applied the Kolmogorov-Smirnov test to the whole WD sample as well as to sub-samples of different magnitude bins, we found that the distribution of WDs in the solar neighbourhood is consistent with being uniform and that the 25 pc WD sample can be regarded as statistically complete. Therefore, this eliminates the possible concern that the shape and the location of the cut-off of the observational WD luminosity function are affected by a Malmquist bias (e.g. Liebert et al. 1979; Iben & Tutukov 1984; García-Berro & Oswalt 2016). We emphasise that in our completeness assessment we refer to the sample of single or resolved WDs. As for unresolved companions, it is plausible to speculate that our sample is more incomplete, which affects the derived number density of WDs in the solar neighbourhood.

We also assessed the sky distribution of all stars in the CNS5 within the completeness limit and observe that their distribution is not only homogeneous but also isotropic. However, the distribution of ultra-cool dwarfs in our catalogue with distances beyond the completeness limit has a smaller density in the Galactic plane than outside of it. This indicates that the majority of missing brown dwarfs are probably hiding in the Galactic plane regions. Recently, Best et al. (2021) performed a detailed analysis of anisotropies of brown dwarfs over the sky. Similarly to what we observe, they concluded that their sample shows a deficiency of brown dwarfs at low Galactic latitudes.

5.3. Luminosity functions

5.3.1. Main-sequence luminosity functions

In this section, we illustrate that the CNS5 provides an excellent sample to derive the observational luminosity functions in optical as well as in MIR wavelengths. As a first step, we want to separate our sample into WDs and main-sequence stars. WDs were selected using criteria defined in Eq. (10). The following limit was used to separate red giants (RG) from the main-sequence stars:

(i) $M_G < -6.2$ mag $+ 15(G - RP)$
(ii) $M_G < 4.3$ mag

As a result of these cuts (see Fig. 11), we obtain a total of 20 RGs and 264 WDs. All the remaining objects are assumed to belong to the main sequence.

As demonstrated in the previous section, the CNS5 catalogue is complete down to 19.7 mag in the $G$ band. Therefore, the completeness correction was not required there. However, to
to reveal the star formation history of the solar neighbourhood. Thus, inverting the observational WDLF allows us to determine the age of the local stellar population (Schmidt 1959). The finite age of the population, are dependent not only on the adopted WD evolutionary models, but also sensitive to the properties of the observational dataset which is used to derive the WDLF. Therefore, the observational WDLF will better correspond to reality when derived from a volume-limited sample with maximised completeness and where the absolute magnitudes are estimated using parallaxes with excellent precision and accuracy and not from reduced proper motions as was done in the past (e.g. Harris et al. 2006).

Such a sample of WDs is provided by the CNS5. Thus, we derive the observational WDLF in Gaia’s G band using the same approach as outlined above for main-sequence stars. The derived luminosity function is shown in Fig. 14.

The total number density is another important parameter for describing a local WD population and is also used for the normalisation of the theoretical WDLFs. The CNS5 contains 264 WDs within the 25 pc volume. This translates into a total number density of \((4.03 \pm 0.25) \times 10^{-3}\) stars pc\(^{-3}\). Our result is consistent with previous findings (Liebert et al. 2005; Gaia Collaboration 2021b).

6. Discussion and outlook

We first assess the overall completeness of the CNS5 based on the completeness limits derived in Sect. 5.2. From Fig. 10, we estimate that we statistically include all systems in the 25 pc volume with absolute G magnitudes brighter than about 19.7 mag (or absolute W1 magnitudes brighter than 11.8 mag), corresponding to a spectral type of about L8 (Dupuy & Liu 2012; Pecaut & Mamajek 2013). Thus, the CNS5 contains virtually all main-sequence stars as well as virtually all brown dwarfs up to spectral type L8. We stress that our completeness assessment refers to well-resolved components in case of binary or multiple stars; the CNS5 is more incomplete when it comes to the identification of companions, especially those of low mass or of close separation.

Since we derived the completeness limit in a statistical sense, namely by judging from the density of objects in smaller and closer volumes to larger and more distant volumes, we do not claim that every single system is indeed listed, but the number of missing systems should be rather small compared to the number of objects listed in the catalogue.

8 Updates available at https://www.pas.rochester.edu/~emamajek/EEM_dwarf_UBVIJK_colors_Teff.txt
This is a major step forward; previous completeness limits for brown dwarfs in particular, but also for M dwarfs, were much closer than the 25 pc distance. The larger volume and larger number of objects that come with an increased completeness radius enable statistical studies with much smaller error bars.

Previously, RECONS (Henry et al. 2016) had listed 366 objects within the 10 pc sample, which they estimated was 90% complete. The CNS5 has added 26 objects within the 10 pc volume, which now contains 392 objects with parallaxes larger than or equal to 100 mas. Even when compared to the GCNS and considering the 3σ confidence interval of the parallaxes, the CNS5 lists 108 more objects within the 10 pc and 739 more within the 25 pc volume because it includes not only Gaia data, but also HIPPARCOS for the bright stars otherwise missing in Gaia as well as the infrared ground-based parallax survey from Best et al. (2021); Kirkpatrick et al. (2021), which helps tremendously with the completeness of sub-stellar objects.

When comparing the CNS5 with the 10 pc sample from Reylé et al. (2021), we found that the CNS5 adds only two objects not listed in the 10 pc sample, presumably due to the different selection approaches used. Conversely, 148 sources from their 10 pc sample are missing in the CNS5 because they are either an exoplanet, a component of an unresolved binary (these will be part of the CNS6), or if they have a parallax uncertainty $\sigma_{\pi} > 10$ mas or if their parallax was just an estimate without uncertainty (such as CWISE J061741.79+194512.8 AB).

The CNS5 contains 5931 objects in total. Among them, there are 5230 stars (including the Sun, 20 giant stars, and 264 WDs) and 701 brown dwarfs. Here, we assume that the approximate stellar-to-sub-stellar boundary lies at $80 M_{\text{Jup}} = 0.076 M_\odot$, corresponding to spectral type L1 ($M_\odot = 16.90$ mag or $W1 - W2 = 0.28$ mag). This yields a stellar number density of $(7.99 \pm 0.11) \times 10^{-2}$ stars pc$^{-3}$, while the number density for brown dwarfs is $(1.07 \pm 0.04) \times 10^{-2}$ objects pc$^{-3}$.

About 72% of stars (or ≈63% of stars and brown dwarfs) in the CNS5 are M dwarfs (there are 3760 main-sequence stars in the 10 pc sample). The fraction of M-dwarfs in the 10 pc sample was found to be ~61% (Reylé et al. 2021). The number of M-dwarfs within the 25 pc volume could still change in the future, in particular due to unresolved multiple systems in the CNS5.

Another interesting quantity is the fraction of stars relative to the fraction of brown dwarfs, which is directly related to the star formation process. Previous estimates included a factor of six times more stars than brown dwarfs in the 8 pc volume by Kirkpatrick et al. (2012), ten times more stars than brown dwarfs in the 10 pc volume from the RECONS project Henry et al. (2016), and a factor of 5.2 from Bilain & Scholz (2016) within 6.5 pc, while newer estimates seem to converge at a factor of around 6–7 Kirkpatrick et al. (2019); Henry et al. (2019). There are 4.4 stars per each brown dwarf listed in the 10 pc sample from Reylé et al. (2021). In the CNS5, the ratio of stars to brown dwarfs is 4.6 ± 0.4 for the 15 pc volume and is consistent with the values derived for smaller volumes (see Table 4). Within the total volume of 25 pc, the factor is 7.5 ± 0.3, indicating that more brown dwarfs than stars are missing at greater distances.

The brown dwarf census is still somewhat limited. Assuming the star-to-brown dwarf ratio is about 5, we can estimate an approximate number of brown dwarfs currently missing. Knowing that there are 5230 stars in the 25 pc volume, one would expect 1046 brown dwarfs in the same volume. As mentioned above, 701 of them are listed in the CNS5, so about 345 brown dwarfs are missing. Therefore, we conclude that about one third of brown dwarfs, corresponding to about 6% of all objects within 25 pc, are still to be discovered.

In Sect. 5.2, we show that the WD sample in the CNS5 is statistically complete within 25 pc. We derive a number density of WDs of $(4.03 \pm 0.25) \times 10^{-3}$ stars pc$^{-3}$. Thus, white dwarfs represent 5% of the local stellar population. We do not see a single faint blue WD as seen by Scholz (2022), but there are only 59 such objects in the GCNS, so our volume of 25 pc might be too small to include one of these rare objects.

Similarly, we do not clearly see the Jao gap (Jao et al. 2018) at absolute G magnitudes of 10.14 mag, although one could notice a small feature if looking closely. The gap becomes more prominent only if looking at larger volumes; it is visible in the GCNS (Gaia Collaboration 2021b).

We plan to compile another version of the CNS, termed CNS6, based on Gaia DR3 in the future. In particular, we will include more information on multiplicity, including spec-troscopic companions from the literature and homogeneously derived stellar parameters for all objects in the catalogue.

The CNS5 catalogue also provides the opportunity to investigate the exoplanet inventory in a sample that is unbiased with regard to spectral type or apparent magnitude, in contrast to other typical planet search samples. The planet population within 25 pc might be more representative of the overall planet population in the Milky Way - at least in those environments that resemble the solar neighbourhood - than just the overall known planet population, which is highly biased by the sensitivities of the various planet search methods. Furthermore, the astrometric method is most sensitive around the most nearby stars and thus ideally complements our knowledge about exoplanets in the nearby stars sample, which so far mainly comes from the transit and radial velocity methods. Since astrometry is most sensitive at intermediate periods or semi-major axes, it ideally complements the transit and radial velocity methods that are most sensitive to the shortest periods, and direct imaging detections at the widest separations. Significant contributions regarding intermediate period/semi-major axis planets in the nearby stars sample are expected, especially from Gaia DR4, which will also contain epoch astrometry.

**Table 4. Star-to-brown dwarf ratio in the CNS5 for different distance limits.**

| $r$  | # of stars | # of BDs | Total | Stars/BDs |
|------|------------|----------|-------|-----------|
| 6.5 pc | 116        | 22       | 138   | 5.3 ± 1.4 |
| 8.0 pc | 164        | 40       | 204   | 4.1 ± 0.8 |
| 10 pc  | 319        | 74       | 393   | 4.3 ± 0.6 |
| 15 pc  | 1066       | 231      | 1297  | 4.6 ± 0.4 |
| 20 pc  | 2590       | 413      | 3003  | 6.3 ± 0.3 |
| 25 pc  | 5230       | 701      | 5931  | 7.5 ± 0.3 |

**Notes.** The ratio increases significantly at distances larger than 15 pc, indicating that more brown dwarfs than stars are missing at larger distances.

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Appendix A: Selecting astrometrically clean datasets from Gaia EDR3

Data selection from Gaia EDR3 is compromised by the presence of sources with spurious astrometric solutions in the published catalogue. In this section, we discuss our quality cut, which eliminates these sources. The validation of this approach follows in the next subsection.

There is no unique selection criterion (or combination of criteria) that would differentiate between sources with spurious and reliable astrometric solutions in Gaia EDR3 for every use case. For each specific task, one should choose appropriate selection criteria individually. Our aim is to define a cut that is conservative enough to only retrieve objects with reliable astrometry (parallaxes in particular). At the same time, the adopted cut should not lessen the completeness of our sample by removing objects that do have reliable parallaxes but with inconsistencies in photometry or even with null values of G, BP, or RP fluxes.

The RUWE (re-normalised unit weight error; Lindegren 2018) and photometric excess factor (Evans et al. 2018; Lindegren et al. 2018; phot_bp_rp_excess_factor in the Gaia EDR3 catalogue) are the two most widely used parameters in various selection criteria. Deriving both of these parameters involves photometric measurements: the re-normalisation factor of the RUWE depends on the magnitude and colour of the source, and photometric excess is defined as the flux ratio \((I_{BP} + I_{RP})/I_G\). A deviation from the expected flux excess indicates inconsistency between G, BP, and RP photometry and is therefore often used to exclude such sources. However, one should keep in mind that this metric does not reveal the origin of the inconsistency: it is not possible to distinguish between objects where only BP and RP fluxes from the Gaia photometric instrument are affected and objects where the G flux from the astrometric field is problematic too.

It was shown that both parameters can reach high values for sources with peculiarities in their photometry: an excess in the RUWE can be induced by photometric variability or by the presence of an unresolved companion (Belokurov et al. 2020), while the photometric excess factor tends to be larger for objects with peculiar SEDs as well as for various types of variable stars (Riello et al. 2021). Therefore, making the decision whether to include an object in the catalogue based on photometric excess or RUWE would bias our catalogue against such types of objects.

We recall that spurious solutions are often caused by mistakes in cross-matching of individual measurements when assigning the source_id. Measurements of two (or more) different objects associated with the same source_id will result in a spurious catalogue entry; the pipeline interprets the measured displacement as an apparent motion of the object and describes it through a non-physical astrometric solution. This leads to a spuriously large parallax, yet with relatively large formal uncertainties (as a consequence of large centroid dispersion). Obviously, such confusion occurs mostly in crowded fields, for instance, close to the Galactic plane and the Magellanic clouds. This is illustrated by Fig. A.1 (top panel), where an overdensity along the Galactic plane is clearly visible in the sky distribution of the sample (hereafter, 25 pc sample) retrieved by selecting all objects from Gaia EDR3 satisfying Eq. (1).

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Given the above, we can expect a dichotomy between spurious and reliable astrometric solutions in the \((\Delta \text{GoF}, \sigma/\sigma_m)\) parameter space. This dichotomy is shown for the 50 pc sample in Fig. A.2: sources with spurious solutions (the cluster of points in the top left corner) are well separated from the sources with reliable astrometric solutions.

For an astrometric solution to be considered reliable, we require the source to satisfy Eq. (2), reproduced here for convenience:

\[
A_{\text{GoF}} < 10^{-5.12} \left(\frac{\sigma}{\sigma_m}\right)^{2.61},
\]

where \(c_0, c_2, s_2\) are Fourier coefficients. If an object is a binary, this will be indicated by a large amplitude of the IPD GoF (ipd_gof_harmonic_amplitude in Gaia EDR3), which indicates the level of asymmetry in the image and is computed as:

\[
\text{GoF} = c_0 + c_2 \cos(2\psi) + s_2 \sin(2\psi).
\]

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For an astrometric solution to be considered reliable, we require the source to satisfy Eq. (2), reproduced here for convenience:

\[
A_{\text{GoF}} < 10^{-5.12} \left(\frac{\sigma}{\sigma_m}\right)^{2.61},
\]
Where \( \sigma/\sigma_0 \) corresponds to \texttt{parallax\_over\_error} as published in the \textit{Gaia} EDR3 catalogue; that is, parallax zero-point corrections or error inflation are not taken into account for this selection. Here, the slope of the line is chosen so that it follows beneath the cluster of sources with spurious solutions. However, this approach comes with its limitation: it works best for nearby stars and it is only applicable in the high-S/N regime. In other words, the cut is tailored to objects with significant parallaxes, where \( \sigma/\sigma_0 \) is larger than that of sources with spurious astrometric solution. For more distant sources (Fig. A.2, cf. Fig. 1), the parallax-over-error ratio decreases, the valley between the clusters of spurious and reliable solutions becomes less clean, and the slope of the cut has to be adjusted in each individual case according to demands for completeness and purity.

Figure A.3 illustrates that the widely used cut \texttt{RUWE} $< 1.4$ is not an optimal approach when completeness of a sample is important. A large number of objects, especially at magnitudes around \( G \approx 12 \) mag, have small amplitudes of the IPD GoF (below the threshold defined by Eq. (A.3)), but would otherwise have been removed by the cut on the RUWE. On the other hand, we should note the presence of spurious objects with \( G \approx 20 \) mag with \texttt{RUWE} $< 1.4$. Including them in the sample would contaminate CNS5 and yield an overestimated completeness and distorted luminosity function.

Appendix A.1: Selection criterion validation

In the following, we examine whether \texttt{ipd\_gof\_harmonic\_amplitude} and \texttt{parallax\_over\_error} are sufficient to define a rigorous selection criterion for objects with significant parallaxes to eliminate spurious astrometric solutions in \textit{Gaia} EDR3 and whether such selection criterion yields results as good as with other classifiers which are in use.

Appendix A.1.1: ‘Fidelity’ from Rybizki et al. (2022)

Rybizki et al. (2022) used machine learning to classify astrometric solutions in \textit{Gaia} EDR3 and to eliminate spurious solutions. They trained a neural network using 17 parameters from \textit{Gaia} EDR3 (including \texttt{ipd\_gof\_harmonic\_amplitude} and \texttt{parallax\_over\_error}) and provided an ‘astrometric fidelity’ for each source - a parameter with values in the range between 0 (spurious solution) and 1 (reliable solution). This approach is somewhat similar to what has been done for the GCNS, now extended to the entire data release.

Here, we validate our cut on harmonic amplitude against the updated version of the classifier (\texttt{fidelity\_v2} column in the \texttt{gedr3spur\_main} table\(^9\)). The principal differences between the original (v1) and the updated (v2) classifier are the new high-density training data and cross-matching of the training sample to Pan-STARRS1 instead of to 2MASS in order to avoid bias against faint blue objects (Rybizki et al. 2022).

Figure A.4 illustrates the remarkable agreement between our cut and the fidelity parameter. Of the 5184 objects classified as good by us, only eight have a fidelity of $< 0.9$, while there are only nine sources with a fidelity of $> 0.9$ rejected by our cut. Hence, we conclude that in 99.84% of the cases the cut on

\(^9\) Hosted at the German Astrophysical Virtual Observatory (GAVO; \url{https://dc.zah.uni-heidelberg.de/}).
If the cut was perfect it would reject all the objects from the cut, and evaluate whether this fraction is statistically significant.

sources with spurious solutions, which are not filtered out by the cut (indicated by the blue solid line).

Appendix A.1.2: Sample with negative parallaxes

The performance of a selection criterion for a particular sample can be assessed through a control sample of sources with spurious astrometric solutions. Such a control sample can be constructed under the fundamental assumption that the probability of positive or negative parallax in a spurious solution is approximately equal; that is, the probability density function is symmetric around $\sigma = 0$. Assuming this symmetry and the fact that any astrometric solution with a highly negative parallax (i.e. a negative parallax where the deviation from zero is statistically significant) is spurious by definition, we can estimate the number of sources with spurious solutions in our sample of objects with positive parallaxes (Fabricius et al. 2021). Additional support for this approach comes from Gaia Collaboration (2021b); using the large negative parallax sample, they constructed the training set for a random forest classifier and utilised it to generate the GCNS. That being said, we select the control sample symmetrically to Eq. (1):

$$\sigma - 3\sigma_{\text{err}} \leq -40 \, \text{mas}. \quad (A.4)$$

The resulting sample contains 630 objects.

Consequently, when we apply our cut on harmonic amplitude (Eq. (A.3)) to the control sample we may infer the fraction of sources with spurious solutions, which are not filtered out by the cut, and evaluate whether this fraction is statistically significant. If the cut was perfect it would reject all the objects from the control sample.

In Fig. A.5 we show the control sample of sources with spurious solutions in the $\text{ipd\_gof\_harmonic\_amplitude, } |\sigma/\sigma_{\text{err}}|$ parameter space (red markers), whilst the 25 pc sample is shown in the background (grey markers). As expected, the vast majority of the sources in the control sample have large amplitude of the IPD GoF and low (absolute) values of the parallax_over_error. Therefore, these sources do not satisfy the condition in Eq. (A.3) and thus are filtered out by our cut (indicated by the blue solid line).

Here, only four sources are erroneously retained by our cut. This corresponds to 0.63% of the control sample and is well below the Poisson noise: $\sqrt{N} = 25.1$. These results allow us to conclude that the cut works as intended.

Appendix A.1.3: GCNS

Here, we compare our classifier with the classifier used to generate the GCNS. As outlined in Sect. 2.2.3, sources in the GCNS were selected from Gaia EDR3 using supervised machine-learning. Specifically, the removal of sources with spurious solutions was done with a random forest classifier that included 14 predictive variables (Gaia Collaboration 2021b).

To validate our selection criterion in Eq. (A.3), we used the sample of sources in the GCNS that are possibly located within 25 pc of the Sun. These are the sources that satisfy our Eq. (1). There are 5191 such sources in the GCNS.

When comparing both datasets, we find that there are five sources included in our sample that are rejected in the GCNS. What these sources have in common is a relatively low flux-over-error ratio (especially in $RP$ band) and, in addition, either 100% of their transits flagged as blended in the $BP$ and $RP$ bands (four sources) or there is no $BP$ and $G$ photometry at all, while 15 out of 20 $RP$ transits are flagged as blended (one source). However, as we discuss in Appendix B, issues with $BP$ and $RP$ photometry, including blending, do not necessarily imply that the astrometric solution is spurious since the astrometric solution in Gaia is obtained using data from the CCDs in the astrometric field, whereas $BP$ and $RP$ fluxes are derived from the integration of the $BP$ and $RP$ low-resolution spectra.

On the other hand, 12 sources that are included in the GCNS (0.2% of the GCNS 25 pc sample) are rejected by our classifier as they have a high harmonic amplitude and low parallax-over-error ratio. Possible causes include extreme magnitudes (three sources have magnitudes in the range of $2.09 \leq G \leq 4.95$ mag, whereas the remaining nine sources are fainter than $G \geq 19.69$ mag) and the probable binarity of these sources. The list of these sources and their properties is shown in Table A.1. All sources in the sample have a counterpart in 2MASS. Five of the sources are indeed known binaries. Given the colour of the remaining seven sources and their excessive IPD GoF harmonic amplitude, these sources are promising candidates when hunting for nearby brown dwarf binaries, especially with high-resolution imaging surveys.

Overall, the selection with the cut on harmonic amplitude is consistent with the GCNS classifier in 99.8% of the cases when limited to the 25 pc volume.
Appendix B: Deblended G-RP colour

The BP fluxes of faint sources published in Gaia EDR3 are often overestimated due to the low flux threshold problem (Riello et al. 2021; Gaia Collaboration 2021a). Consequently, such objects appear to be bluer in $BP−RP$ or $BP−G$ colours. Another impact of this issue is the reduced measured scatter in the $BP$-band for these sources.

Furthermore, the S/N for the vast majority of objects is significantly higher in the $RP$-band than that in the $BP$-band (Fig. B.1). Thus, the use of the $G − RP$ colour is often favoured over the $BP − RP$ (e.g. Scholz 2020; Kaltenegger & Faherty 2021) to name a few.

However, when a CMD is plotted against the $G − RP$ colour, a substantial number of objects show an offset towards the red from the main sequence. Neither the number of such outliers nor their position on a CMD can be explained by the object’s intrinsic properties, such as age, metallicity, or binarity, or a combination thereof. These offsets are also not consistent with expected numbers and positions of pre-main-sequence stars.

We recall that the $BP$ and $RP$ fluxes are the integrated mean fluxes from the Gaia photometric instrument, and these fluxes are obtained from CCD windows of $3.5'' × 2.1''$ downlinked to Earth, whereas the broad-band $G$ flux is determined from PSF or LSF fitting to an object window from the astrometric field (AF) CCDs (Busso et al. 2021).

If there is an additional object in the window of the source (e.g. due to a crowded field or a binary), the measured flux will be affected by blending and the flux value will be overestimated. This primarily affects $BP$ and $RP$ bands; contamination in the $G$ band is rather infrequent due to the smaller AF window size ($0.72'' × 2.1''$; Gaia Collaboration et al. 2016).

With this in mind, when using the $G − RP$ colour – that is, combining unbiased $G$ flux with the overestimated $RP$ flux – blended sources or poorly resolved binaries should appear redder than well-behaved single sources, just as observed in a CMD using $G − RP$ on the abscissa.

Affected sources can be identified without prior knowledge of their position in a CMD. For instance, the impact of blending can be assessed with a metric defined as a simple ratio between the total number of blended transits in both $BP$ and $RP$ bands and the total number of observations in these bands (Riello et al. 2021):

$$\beta = \frac{N_{BP\_blended} + N_{RP\_blended}}{N_{BP} + N_{RP}},$$ (B.1)

where $N_{BP\_blended}$ and $N_{RP\_blended}$ correspond to the number of transits flagged as blended in the $BP$ and $RP$ bands, respectively ($phot\_bp\_n\_blended\_transits$ and $phot\_rp\_n\_blended\_transits$ columns in the Gaia EDR3 $gaia\_source$ table), while $N_{BP}$ and $N_{RP}$ are the total number of observations that were used to compute the integrated mean flux and its error in the $BP$ and $RP$ bands, respectively ($phot\_bp\_n\_obs$ and $phot\_rp\_n\_obs$ columns in Gaia EDR3).

Furthermore, Gaia EDR3 contains various quality indicators that hint at the possibility that an object is a semi-resolved binary (optical or physical). In particular, $ipd\_frac\_multi\_peak$ corresponds to the percentage of windows where more than one peak was detected by the image parameter determination (IPD) algorithm (Lindegren et al. 2021b).

In Fig. B.2, we demonstrate that the outliers discussed above can indeed be attributed to inconsistencies in the photometry of blended objects (top panel) or poorly resolved binaries (bottom panel), or both. Even though deblending and decontamination...
For this calibration, it is of fundamental importance to only select objects with excellent photometry, whereas the completeness of the sample is not crucial. Therefore, we applied additional, stricter cuts on the astrometrically clean dataset.

We only selected sources with high S/N in both the $BP$ and $RP$ bands ($S/N > 20$; the threshold is denoted by the grey lines in Fig. B.1). Furthermore, we excluded bright objects severely affected by saturation; namely, we only considered sources with $G > 6$ mag (Lindgren et al. 2021b; Riello et al. 2021).

To ensure that we had a sample of excellent data, we only selected sources with five-parameter astrometric solutions in Gaia EDR3. This way we also avoid systematic effects due to the uncertainty of the $G$-band corrections for the sources with six-parameter astrometric solutions (Riello et al. 2021).

Blended sources and (poorly) resolved binaries were removed by applying cuts to the blending metric $\beta$ and the $\text{ipd}_\text{frac}_\text{multi}_\text{peak}$ statistic. Furthermore, we excluded WDs from our sample due to their larger scatter in colour-colour diagram and limited our sample to colours in the $0.0 \text{ mag} \leq (BP - RP) \leq 4.25 \text{ mag}$ range. Outside of this range the data density drops significantly, and, consequently, this would yield an unreliable fit for sources with extreme colours.

To summarise, we constructed the initial sample by applying the following selection criteria:

\begin{align*}
\text{(i)} & \quad \sigma > 10 \text{ mas} \\
\text{(ii)} & \quad \text{Eq. (2): } A_{\text{GOF}} < 10^{-5.12} (\sigma/\sigma_{\text{err}})^{2.61} \\
\text{(iii)} & \quad \text{phot}_{BP}\text{mean}_\text{flux}_{\text{over}}_{\text{error}} > 20 \\
\text{(iv)} & \quad \text{phot}_{RP}\text{mean}_\text{flux}_{\text{over}}_{\text{error}} > 20 \\
\text{(v)} & \quad G > 6.0 \text{ mag} \\
\text{(vi)} & \quad \astrometric\text{params}_{\text{solved}} = 31 \\
\text{(vii)} & \quad \beta < 0.1 \\
\text{(viii)} & \quad \text{ipd}_\text{frac}_\text{multi}_\text{peak} \leq 2.0 \\
\text{(ix)} & \quad M_G > 10.0 \text{ mag } + 2.5(BP - RP) \\
\text{(x)} & \quad 0.0 \text{ mag} \leq (BP - RP) \leq 4.25 \text{ mag}
\end{align*}

Finally, in order to obtain a more robust statistics, we constructed a truncated sample by using the $BP$ and $RP$ excess factor (phot$_{BP}\text{rp}_{\text{excess}}\text{factor}$ in the Gaia EDR3 catalogue) for deriving a trimmed estimator. This is done by splitting the initial sample (grey points in Fig. B.3, top panel) into bins of 0.005 mag in the $BP - RP$ colour and only retaining objects with $BP$ and $RP$ excesses within the interquartile range (IQR) values of phot$_{BP}\text{rp}_{\text{excess}}\text{factor}$ estimated for each of these bins. There are 91,285 sources in the resulting sample (the coloured part of Fig. B.3). The sample only contains sources with high-quality photometry.

In the next step, we derived an empirical model for the synthetic $G - RP$ colour, where input is $BP - RP$ in colour. The aim is to mitigate the inconsistencies between $G$ and $RP$ photometry caused by blending or marginally resolved binaries.

To derive the fit of $G - RP$ for isolated, well-behaved sources, we used cubic splines with 500 equally spaced knots. Even though 500 knots seems like a large number, this is still an appropriate choice given the large size of our sample (each knot contains ~ 180 data points). Furthermore, we wish to emphasise that in our case reducing the interpolation error and thus obtaining smaller residuals is more important than avoiding the problem of overfitting.

The residuals of the derived relationship are shown in Fig. B.3 (bottom panel). They are very small, do not show significant dependence on the $G$, $BP$, or $RP$ fluxes, and are well inside of the window. A few extreme outliers are outside of the frame.
any systematics, and illustrate the high quality of the derived relationship. The RMS error is 0.0013 mag.

The derived relationship is applicable in the $0.0 \text{ mag} < BP - RP < 4.25 \text{ mag}$ range. Another constraint to be considered when applying the relationship is the S/N of $BP$ and $RP$ fluxes in the input. Including sources with a low S/N will lead to unreliable $G - RP$ estimates. Thus, to avoid this, we adopted $S/N = 20$ as the optimal threshold value.

To illustrate the power of the suggested correction, CMDs before and after deblending are shown for the 50 pc sample (Fig. B.4). The colour-coding indicates the difference between the catalogued and deblended values of $G - RP$. When a CMD is plotted against the catalogued (i.e. uncorrected) $G - RP$ colour values, the objects with large residuals appear mostly at unexpected regions of the diagram (Fig. B.4, top panel), and their position in a CMD is not determined by intrinsic properties of an object, but is a consequence of inconsistency in photometry. However, when the deblended colour is used (Fig. B.4, bottom panel), they are located in the expected regions of a CMD. Here, we stress that the objects with peculiar positions in the top panel were not removed, but are plotted with the deblended $G - RP$ colour and are now located on the main sequence, WD sequence, and in the red clump region.

Deblended values of $G - RP$ are listed in the CNS5 for all objects with colours within the applicability range and with sufficient S/N of $BP$ and $RP$ fluxes. We provide the derived spline coefficients and a python function to calculate deblended $G - RP$ values\(^1\). Deblending colours and magnitudes for objects with inconsistencies in photometry is crucial for correct object classification based on the position in the CMD, estimating effective temperatures and fitting isochrones.

\(^1\) https://github.com/AlexGolovin/gaiaedr3_g_rp_synthetic