Low-Frequency Divergence of Circular Photomagnetic Effect in Topological Semimetals

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Novel fermions with relativistic linear dispersion can emerge as low-energy excitations in topological semimetal materials. Here, we show that the orbital moment contribution in the circular photomagnetic effect for these topological semimetals exhibit an unconventional \( \omega^{-1} \) frequency scaling, leading to significantly enhanced response in the low frequency window, which can be orders of magnitude larger than previous observations on conventional materials. Furthermore, the response tensor is directly connected to the Chern numbers of the emergent fermions, manifesting their topological character. Our work reveals a new signature of topological semimetals and suggests them as promising platforms for optoelectronics and spintronics applications.

Topological semimetals, which host unconventional emergent fermion modes around band nodal points at the Fermi level, have been a focus of research in recent years [1–4]. For example, in a Weyl semimetal, the electrons around the so-called Weyl nodal points acquire a relativistic linear dispersion and are described by the Weyl Hamiltonian with an emergent pseudospin-1/2 structure [5, 6]. Recent studies showed that generalizations of Weyl fermions with higher pseudospins of the form \( \sim k \cdot \mathbf{S} \) also exist in crystalline materials and can be engineered in artificial structures [7–11]. The unusual linear dispersion, the pseudospin structure, and the possible topological charge of these emergent fermions should exhibit unique signatures in many physical phenomena [12–20], and this constitutes a main topic of current research on topological semimetals.

Circularly polarized light is a powerful probe of band topology [21–23]. As shown by de Juan et al. [24], it generates in Weyl semimetals a quantized injection current contribution to the circular photogalvanic effect, and the result can be extended to higher pseudospin cases [25]. Since circularly polarized light carries an intrinsic angular momentum, its absorption in a material can generate a magnetization. This circular photomagnetic effect (CPME), also known as the inverse Faraday effect [26–34] or nonlinear Edelstein effect [35], has recently been considered in Weyl semimetals [36–40]. Notably, Gao et al. found that the spin contribution to CPME in Weyl semimetals is frequency independent (\( \sim \omega^0 \)) and manifests the topological structure of Weyl fermions [39].

In this work, we show that the orbital moment contribution to CPME, while vanishing for Weyl fermions, can generate a significant magnetization in topological semimetals with higher pseudospin fermions. Importantly, the result has a \( \omega^{-1} \) scaling hence exhibits a low-frequency divergence, which makes it dominant at low frequencies. Moreover, we reveal that the response tensor can be expressed in terms of the Chern numbers of bands involved in the optical transitions, exhibiting the topological character of the system. The corrections due to lattice effect and the spin contribution are discussed and found to be subdominant in the low frequency window. Based on realistic parameters, the resulting magnetization can reach \( 1 \mu_B/\text{mm}^2 \) under an infrared light with intensity of \( 10^{12} \text{ W/m}^2 \), which can be readily detected in experiment. Our work discovers a nonlinear optical signature of topological semimetals and suggests these materials as promising platforms for opto-spintronics.

**General formula.** We consider a three-dimensional (3D) nonmagnetic solid under the irradiation of a circularly polarized light with frequency \( \omega \). The induced magnetization corresponding to CPME should flip its

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**FIG. 1. Sketch of CPME in topological semimetals with emergent relativistic fermion.** Under a circular polarized light, a static magnetization can be generated. In this case, the product of frequency \( \omega \) with response tensor \( \beta(\omega) \) shows a flat plateau at low energies.
sign under the reversal of circular polarization. It can be generally expressed as

$$M_a = \beta_{ab} (\omega) \left| I_E (\omega) \times E (-\omega) \right|_b,$$  \hspace{1cm} (1)

where $E$ is the electric field of light, $\beta$ is the CPME response tensor, and the subscripts $a$ and $b$ label the Cartesian components. The expression of $\beta$ can be derived by using the second-order perturbation theory. In general, there are both spin and orbital contributions to the induced magnetization. In this work, our focus is on the orbital moment contribution is expected to be significant for topological semimetals with higher pseudospin fermions. Nevertheless, as we will show below, the effect is significantly enhanced for topological semimetals with higher pseudospin fermions.

Scaling relation for linear fermions. Before doing any detailed calculations, we first argue that the response tensor in Eq. (2) follows a $\omega^{-1}$ frequency scaling for higher pseudospin fermions due to their relativistic linear dispersion.

Consider a generic effective Hamiltonian for emergent fermions with linear dispersion:

$$H = k \cdot \Gamma,$$  \hspace{1cm} (4)

where $k$ is the momentum measured from the nodal point, and $\Gamma$ is a vector of $k$-independent matrices with dimension corresponding to the degeneracy of the nodal point. A crucial feature here is that the eigenstate $|u_{nk}\rangle$ only depends on direction of $k$ vector, i.e., $k$, but not its magnitude $k$.

Let’s consider the following scaling transformation in momentum and frequency:

$$k \rightarrow k' = \lambda k, \hspace{0.5cm} \omega \rightarrow \omega' = \lambda \omega,$$  \hspace{1cm} (5)

with $\lambda$ a real number. For the linearly dispersing fermions in (4), one has $H(\lambda k) = \lambda H(k)$ and $\varepsilon_{m, \lambda k} = \lambda \varepsilon_{m, k}$. Moreover, due to the feature noted above, the eigenstates remain invariant under this rescaling, i.e., $|u_{n, \lambda k}\rangle = |u_{nk}\rangle$. It follows that in Eq. (2), $R_{mn, \lambda k} = \lambda^{-2} R_{mn, k}$ and $\mu_{mn, \lambda k} = \lambda^{-1} \mu_{mn, k}$. Consider the low-temperature regime, where $f_{nk} \approx \Theta (E_F - \varepsilon_{nk})$ with $\Theta$ the step function and $E_F$ the Fermi energy. Then the 3D integral in Eq. (2) will be reduced to a 2D integral performed over the optical transition surface $S_{OT}$ consisting all the points in the momentum space where the optical transition occurs, i.e., where the quantity $f_{mn, k} \delta (\varepsilon_{mn, k} - \omega)$ is nonzero for some $m$ and $n$. Then one can show that as long as $S$ remains a closed surface enclosing the nodal point under rescaling, the orbital moment CPME tensor follows the simple scaling relation:

$$\beta_{ab}(\lambda \omega) = \lambda^{-1} \beta_{ab}(\omega).$$  \hspace{1cm} (6)

In other words, $\beta_{ab}$ scales as $\omega^{-1}$. If one plots the quantity $\omega \beta_{ab}$ versus frequency, it should exhibit a flat plateau for linear fermions.

There are two remarks about the scaling relation (6). First, the analysis shows that the relation is solely due to the linear dispersion of the emergent fermion. The result is general in that it does not depend on the specific form of the model (the $\Gamma$ matrices), the degree of degeneracy of the nodal point, or the possible anisotropy in the dispersion. Second, the scaling shows that for nodal points sitting at the Fermi level, the CPME can be divergently large at low frequencies. (Obviously, when Fermi energy deviates from the nodal point, the effect has a lower cut-off frequency due to Pauli blocking.) Since spin and other contributions at most have a $\omega^{0}$ scaling at low frequencies, the orbital moment contribution should dominate in this regime [39]. In the following, we perform concrete model calculations to illustrate these points.
the isotropic model. Reduced area element over the optical transition surface. The band is obtained as $\mu_{n} = i \epsilon \nu_{F} k \cdot S$. Here, the Chern number is defined on a closed surface surrounding the nodal point. The orbital moment for the $n$-th band (counted from bottom to top) of the pseudospin-$j$ particle, the Chern number is given by

$$C_n = -2\chi(j + 1 - n)$$

(8)

Here, the Chern number is defined on a closed surface surrounding the nodal point. The orbital moment for the $n$-th band is obtained as $\mu_{n} = e\chi \nu_{F} k / 8 \pi \left[4j(j + 1) - C_n^2\right]$. Interestingly, $\mu_{n}$ depends on the absolute value of $C_n$ but not its sign. Hence, bands with opposite Chern numbers would have the same orbital moment.

The pseudospin-$1/2$ case corresponds to the Weyl fermions, which, as we discussed before, have a vanishing orbital moment contribution. In the following, we will focus on pseudospin-$1$ and $3/2$ fermions. For $j > 3/2$, the qualitative feature of the result remains but the expression gets more complicated, and such nodal points are not directly stabilized by crystalline symmetry [8].

Considering optical transitions for pseudospin-$1$ and $3/2$ fermions, we find that for both cases, the transition is allowed only between the nearest two bands [41]. Moreover, let’s focus on the trace of the CPME tensor in (2), because it can be put into a compact form

$$\text{Tr} [\beta (\omega)] = \frac{\tau}{8\pi^2} \int_{\text{SOT}} dS_{mn,k} \Delta_{mn,k} \cdot R_{mn,k},$$

where $m = n + 1$, $dS_{mn,k} = dS_{mn,k} / |\delta_{k} e_{mn,k}|$ is a reduced area element over the optical transition surface. Meanwhile, the off-diagonal elements of $\beta (\omega)$ vanish for the isotropic model.

For the $n$-th band (counted from bottom to top) of the pseudospin-$j$ fermions, the scaling relation, so here we just take an isotropic Fermi velocity $\nu_{F}$. As mentioned above, the anisotropy does not affect the qualitative feature of the result remains but the expression gets more complicated, and such nodal points are not directly stabilized by crystalline symmetry [8].

The form of the effective Hamiltonian $H_{\text{eff}}$ are explicitly presented in SM [41]. The column with “with SOC” indicates whether the system contains spin-orbit coupling.

| Notation          | SG and Location | $H_{\text{eff}}$ with SOC |
|-------------------|-----------------|--------------------------|
| C-2 TP (spin-1 particle) | 195, Γ, R; 196, Γ; 197, Γ, H; 198, Γ; 199, Γ, H; 207, Γ, R; 208, Γ, R; 209, Γ; 210, Γ; 211, Γ, H; 212, Γ; 213, Γ; 214, Γ, H; | $v_{1} k \cdot S$ | N |
| C-2 TP            | 197, P; 211, P | $v_{1} k \cdot S + v_{2} k \cdot S'$ | N |
| C-2 DP            | 199, P; 214, P | $v_{1} k \cdot S + v_{2} k \cdot S'$ | Y |
| C-4 DP            | Same as spin-1 particle | $v_{1} k \cdot S + v_{2} k \cdot S'$ | Y |

By straightforward calculation, we find that the results for spin-1 and $3/2$ fermions can be put into the following unified form. For $E_{F} < 0$, we have

$$\text{Tr} [\beta] = \frac{\Lambda_0}{\omega} |C_1| (C_1^2 - C_2^2),$$

(10)

and for $E_{F} > 0,$

$$\text{Tr} [\beta] = -\frac{\Lambda_0}{\omega} |C_{2j+1}| (C_{2j+1}^2 - C_{2j}^2),$$

(11)

where $\Lambda_0 = \tau \nu_{F} / (32\pi)$. This result explicitly demonstrates the $\omega^{-1}$ scaling of the $\beta$ tensor. Although the result is given for the trace, it is clear that the scaling holds for each tensor element. In Fig. 2, we plot the result from numerical calculation. The clear exhibition of...
The lattice effect will introduce higher order (in $k$) corrections to the effective model.

For example, let’s consider adding a quadratic correction term $H' \sim k^2$ to the effective Hamiltonian Eq. (4). In the low frequency regime, this term can be treated as a perturbation. The original eigenstate $|\psi_0\rangle$ would be perturbed into $|\psi_1\rangle = |\psi_0\rangle + |\psi'\rangle$ with $|\psi'\rangle \sim k$. Then the correction for $\beta$ scales as $\beta_{ab} \propto \omega^0$ for small $\omega$. Therefore, similar to the spin contribution, the correction from lattice effect is subdominant in the low frequency regime.

To confirm this point, we consider a lattice model of pseudospin-1 fermions and numerically assess the correction from lattice effect. The model belongs to the space group No. 195 and is presented in [41]. Its band structure is plotted in Fig. 3(b). There are two pseudospin-1 nodal points at $\Gamma$ and $\Gamma$ points in the Brillouin zone (see Table I). The two points have opposite chirality. The Chern number for the point at $\Gamma$ (R) point is calculated as $\mathcal{C} = 2$ ($\mathcal{C} = -2$) for the lowest band. From our result in Eq. (10), one expects that the contributions from the two points would add up and a plateau should appear in $\omega \text{Tr}[\beta]$ at low frequencies. This is indeed verified in Fig. 3(c), where for reference we also plot the result from the effective linear model (the red dashed line).

**Discussions.** Experimentally, the large CPME predicted here can be probed by the magneto-optical Kerr microscopy [49, 50]. As an estimation, the induced magnetization can be related to the light intensity as $M = G I$, with $I$ the intensity of the incident light. At time scale $t \gg \tau$, the photoinduced $M$ saturates to a constant value. For a topological semimetal with spin-1 fermions at the Fermi level, we have $G = \frac{16A_0}{\varepsilon_0 c^2 \omega}$, where $\varepsilon_0$ is the vacuum permittivity and $c$ is the speed of light. Taking typical values of $\tau = 1 \text{ ps}$, $v_F = 4 \times 10^5 \text{ m/s}$ (e.g., as in the topological semimetal RhSi [48, 51–53]), and an infrared pump light with $\omega = 0.5 \text{ eV}$, $G$ is estimated as $G \sim 1.3 \times 10^5 \mu_B A^{-1}/\text{W}$. Under a moderate light intensity of $10^{12} \text{ W/m}^2$, the induced magnetization can reach $\sim 1 \mu_B/\text{nm}^2$. This large induced magnetization is at least two orders of magnitude larger than that observed in DyFeO$_3$ [29] or gold nanoparticles [34], hence it is readily detectable in experiment.

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