Production of charged Higgs bosons
of the Minimal Supersymmetric Standard Model
in $b$-quark initiated processes
at the Large Hadron Collider

Stefano Moretti$^{a,b}$ and Kosuke Odagiri$^a$

$^{a)}$ Cavendish Laboratory, University of Cambridge,
Madingley Road, Cambridge CB3 0HE, UK.

$^{b)}$ Dipartimento di Fisica Teorica, Università di Torino,
and I.N.F.N., Sezione di Torino,
Via Pietro Giuria 1, 10125 Torino, Italy.

Abstract

We study integrated and differential rates for the production of charged Higgs bosons $H^\pm$ of the Minimal Supersymmetric Standard Model via $b$-quark initiated subprocesses in $pp$ collisions at the Large Hadron Collider. In detail, we compute cross sections and distributions of the reactions: $bU \to bD H^+ \to bD \tau^+ \nu_\tau \oplus C.C.$ and $bU \to bD H^+ \to bD t \bar{b} \to bD b \bar{b} j j \oplus C.C.$, for a $H^\pm$ scalar in the intermediate (i.e., $M^\pm < m_t + m_b$) and heavy (i.e., $M^\pm > m_t + m_b$) mass range, respectively ($U$ and $D$ represent generic $u$- and $d$-type light quarks). In the first case, a detailed treatment of various possible backgrounds is also given.

Electronic mails: moretti,odagiri@hep.phy.cam.ac.uk
1. Introduction

At the Large Hadron Collider (LHC) \[1, 2\], the charged Higgs boson \(H^\pm\) of the Minimal Supersymmetric Standard Model (MSSM) is expected (if it exists) to be copiously produced in top quarks decays, via the chain \(t \to bH^\pm \to b(\tau \nu_\tau)\), provided that \(m_t > M_{H^\pm} + m_b\) and that the value of \(\tan \beta\) is low or high enough\[4\].

The main decay modes of the \(H^\pm\) scalar are (for \(M_{H^\pm} < m_t + m_b\)) into \(cs, \tau \nu_\tau\) and \(W^\pm h\) pairs, where in the last case \(h \to b\bar{b}\) (\(h\) being the lightest neutral Higgs boson of the MSSM) \[3\]. The first decay is never dominant, whereas the second is overcome by the third in a narrow mass window right before the opening of the \(tb\) Higgs decay threshold, but only at very small values of \(\tan \beta\). Otherwise, the branching ratio \(BR(H^\pm \to \tau \nu_\tau)\) is the largest (around 98\%, for \(\tan \beta > 2\)), and it depends only slightly on the \(\beta\) angle. When \(M_{H^\pm} > m_t + m_b\), the \(H^\pm \to tb\) decay mode is in practise the only relevant one (with a branching ratio of practically 100\%)\[2\].

Extensive studies and simulations for \(H^\pm\) production at the LHC have been carried out \[1, 2\]. Top quarks are produced in \(tt\) pairs, via \(q\bar{q}\) and \(gg\) fusion, with a large cross section (around 500 pb at \(\sqrt{s}_{pp} = 14\) TeV and for \(m_t = 175\) GeV). The signal that has been considered in the ATLAS and CMS Technical Proposals is the one involving one top decaying to a charged Higgs, and the other decaying inclusively (i.e., either via a \(H^\pm\) or, mostly, a \(W^\pm\)) into electrons and muons (and corresponding neutrinos). The charged Higgs boson is searched for by means of the leptonic signature \(H^\pm \to \tau \nu_\tau\).

Since neutrinos in the final state prevent one from reconstructing the Higgs mass from the momenta of its decay products, the existence of \(H^\pm\) signals in the data can be inferred only from an excess of \(\tau\) production with respect to what is predicted for the Standard Model (SM) backgrounds (lepton universality breaking signal). Among the letter, one must number the irreducible ones (non-resonant \(\tau\) production and \(tt\) production followed by \(t \to W^\pm b\) and \(W^\pm \to \tau \nu_\tau\)) as well as the reducible ones (mainly \(tt\) where either a jet from a \(W^\pm\) fakes a \(\tau\) or a \(b\)-jet decays leptonically into or fakes a \(\tau\), but also \(bb\) production followed by \(bb \to \tau +\) jets and \(W^\pm +\) jets, with one of the jets faking a \(\tau\)) \[1, 2\]. By selecting an isolated high \(p_T\) lepton and by requiring one jet to have a high transverse energy together with one \(b\)-tagging should allow one to explore a large portion of the \((M_A, \tan \beta)\) plane, with a significance up to 5\(\sigma\) (assuming a 10 fb\(^{-1}\) integrated luminosity of the collider) \[1\].

It is the purpose of this letter to study other production mechanisms of charged Higgs bosons of the MSSM at the LHC, via subprocesses with \(b\)-quarks in the initial state. In particular, we calculate (for a \(H^\pm\) scalar whose mass is below the \(tb\) threshold) the signal reaction (including charge conjugation)
\[
bU \to bDH^+ \to bD\tau^+\nu_\tau \oplus C.C.,\tag{1}
\]
and the background processes
\[
bU \to bD\tau^+\nu_\tau \oplus C.C.,\tag{2}
\]
via intermediate \(W^\pm, \gamma, Z, H, h, A\).

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1 The minimum of the \(t \to bH^\pm\) decay rate is at about \(\tan \beta = 6\).

2 In the above discussion and throughout this paper we have assumed that the mass scale of the Supersymmetric particles is above the \(H^\pm\) mass, such that only decays into ordinary matter are here considered.
\[ bU \rightarrow bD\tau^+\nu_\tau \oplus C.C., \text{ via intermediate } W^\pm, g, \quad (3) \]

\[ U\bar{D} \rightarrow b\bar{b}\tau^+\nu_\tau \oplus C.C., \text{ via intermediate } W^\pm, g, \quad (4) \]

where \( U(D) \) represents a generic \( u(d) \)-type light quark (i.e., \( u, d, s \) and \( c \)) found inside the proton and \( H, h, A \) are the three neutral Higgs bosons of the MSSM. For a heavy \( H^\pm \), we consider the production and decay chain (again including charge conjugation)

\[ bU \rightarrow bDH^+ \rightarrow bD\bar{b}t \rightarrow bD\bar{b}jj \oplus C.C., \quad (5) \]

assuming that, because of the spectacular signature that is produced in the final state, background processes can easily be kept under control. In reactions (1)–(3) and (5) we treat the initial \( b \)-quark as a constituent of the proton with the appropriate momentum fraction distribution \( f_{b/p}(x, Q^2) \), as given by our default set of partonic structure functions.

The relevance of these reactions can be understood if one considers that:

- at the typical (partonic) energies of the LHC the content of \( b \)-quarks inside the colliding protons is very much enhanced, compared to lower energy hadronic scatterings (such as, e.g., at the Tevatron);

- the presence of \( b \)-quark in initial, virtual and final states means that many of the MSSM Yukawa couplings of the Higgs bosons of the theory are increased for large values of \( \tan \beta \);

- the vertex tagging performances of the LHC detectors are expected to become almost ‘ideal’ by the time the machine starts operations, thus allowing one to greatly reduce the QCD background of light quark and gluon jets.

Finally, we also stress that \( b \)-quark initiated processes at LHC energies have already been demonstrated to be important in the cases of neutral MSSM Higgs production, especially at large \( \tan \beta \)’s and for intermediate masses of the scalars \([4]\), as well as in the case of charged Higgs production, via the reaction \( g\bar{b} \rightarrow H^+t \oplus \) C.C.. \([5]\).

The plan of this paper is as follows. In the next Section we give some details of the calculation and list the values adopted for the various parameters. Section 3 is devoted to a discussion of the results. Conclusions are in Section 4. In the Appendix we write down the amplitudes squared of the signal processes.

## 2. Calculation

To calculate processes (1)–(5) we have used the spinor techniques described in Refs. [6, 7, 8]. The FORTRAN codes we have produced have been counter-checked against the outputs of MadGraph [3], which incorporates the HELAS subroutines [10]. We have always found perfect agreement between the two kinds of programs. The codes written using the helicity formalism of Refs. [6, 7, 8] have also been tested for gauge invariance. Furthermore, in order to speed up the numerical evaluations in Monte Carlo simulations, the matrix elements for the signal processes (1) and (5) have been computed using the textbook method of taking the trace of the gamma matrices, with the help of FORM.
The analytical expressions obtained in this way are very simple, so that we do reproduce them here (see the Appendix). They have been eventually implemented and their numerical results agree with those of the other codes. The integrations over the phase space have been performed using VEGAS [12].

The tree-level Feynman diagrams that one needs for computing processes (1)–(5) are given in Fig. 1a,b,c and d. The labelling of the particles in the figures corresponds to their ordering in the left-hand side (for the initial state) and in the right-hand side (for the final state) of equations (1)–(5). Note that the virtual particle content of the diagrams is explicitly indicated in Fig. 1 for all reactions.

Concerning the values of the various parameters entering in the computation of processes (1)–(5), we have proceeded as follows. First, we have set up the mass scale of the Supersymmetric partners of ordinary matter well above the energy reach of the LHC, such that we can neglect their contribution in our calculations. To further simplify the discussion, we have assumed a universal soft Supersymmetry–breaking mass [13, 14]

\[ m_{\tilde{u}}^2 = m_{\tilde{d}}^2 = m_{\tilde{q}}^2, \]  

and negligible mixing in the stop and sbottom mass matrices,

\[ A_t = A_b = \mu = 0. \]  

One-loop corrections to the masses of the MSSM neutral CP–even Higgs bosons and to the mixing angle \( \alpha \) are introduced via the parameter \( \varepsilon \) of Ref. [14], given by (neglecting the \( b \)-mass)

\[ \varepsilon = \frac{3e^2}{8\pi^2 M_{W^\pm}^2 \sin^2 \theta_W} \left[ \ln \left( 1 + \frac{m_{\tilde{q}}^2}{m_t^2} \right) \right], \]

where \( e^2 = 4\pi \alpha_{em} \). One then gets [13]

\[ M_{h,H}^2 = \frac{1}{2} [M_A^2 + M_Z^2 + \varepsilon / \sin^2 \beta] \]

\[ \pm \left\{ [(M_A^2 - M_Z^2) \cos 2\beta + \varepsilon / \sin^2 \beta]^2 + (M_A^2 + M_Z^2)^2 \sin^2 2\beta \right\}^{1/2}, \]

and

\[ \tan 2\alpha = \frac{(M_A^2 + M_Z^2) \sin 2\beta}{(M_A^2 - M_Z^2) \cos 2\beta + \varepsilon / \sin^2 \beta}. \]

For the MSSM charged Higgs masses we have maintained the tree–level relations

\[ M_{H^\pm}^2 = M_A^2 + M_{W^\pm}^2, \]

since one–loop corrections are small compared to those for the neutral Higgses [14].

In the numerical calculations presented in the next Section we have adopted the following values for the electromagnetic coupling constant and the weak mixing angle: \( \alpha_{em} = 1/128 \) and \( \sin^2 \theta_W = 0.2320 \). The strong coupling constant \( \alpha_s \), which appears at next-to-leading order in the computation of the charged Higgs decay width (see Ref. [3])

\[^3\text{The C.C. diagrams can be obtained by simple crossing and time inversion of fermion lines.}\]
and enters in some of the production mechanisms, has been evaluated at two loops, with
\( \Lambda^{(4)}_{\text{MS}} = 230 \text{ MeV} \), and with the number of active flavours \( N_f \) (and the corresponding
\( \Lambda^{(N_f)}_{\text{MS}} \)) calculated according to the prescription of Ref. [16] at the scale \( Q^2 = s \).

For the gauge boson masses and widths we have taken
\( M_Z = 91.1888 \text{ GeV}, \quad \Gamma_Z = 2.5 \text{ GeV}, \quad M_{W^\pm} = 80.23 \text{ GeV} \) and \( \Gamma_{W^\pm} = 2.08 \text{ GeV} \), while for the fermion masses we have
used
\( m_e = m_{\nu_e} = m_{\nu_\mu} = m_{\nu_\tau} = 0, \quad m_\mu = 0.105 \text{ GeV}, \quad m_\tau = 1.78 \text{ GeV}, \quad m_u = m_d = m_s = m_c = 0, \quad m_b = 4.25 \text{ GeV} \) and \( m_t = 175 \text{ GeV} \), with all widths equal to zero except
for \( \Gamma_t \). We have calculated this at tree–level within the MSSM, using the expressions
given in Refs. [17, 18]. The universal Supersymmetry–breaking squark mass is in the
numerical analysis \( m_\tilde{q} = 1 \text{ TeV} \) and the LHC centre-of-mass (CM) energy is \( \sqrt{s_{pp}} = 14 \text{ TeV} \). Finally, throughout the paper we have always used MRSA [20] as the default set
of partonic distributions, with the same \( \alpha_s \) and \( \Lambda^{(4)}_{\text{MS}} \) as above.

3. Results

As it is impractical to cover all possible regions of the MSSM parameter space
\((M_A, \tan \beta)\), we have decided to concentrate here on the two representative (and ex-
treme) values \( \tan \beta = 1.5 \) and 30, and on masses of the pseudoscalar Higgs boson \( A \)
in the range \( 60 \text{ GeV} \leq M_A \leq 500 \text{ GeV} \). The large bibliography existing on the MSSM
Higgs decay phenomenology allows one to easily extrapolate our results to other values
of \( \tan \beta \) [21].

In Fig. 2 we display the total cross sections at the LHC for processes (1)–(4), for
values of \( M_A \) up to 480 GeV and for the two above-mentioned \( \tan \beta \)'s (note that a
minimum transverse momentum of 10 GeV is required for all detectable particles in
the final states of all processes). The relevant feature of Fig. 2 is that process (1) has
rather large rates, of the same order as the backgrounds (2)–(4). This is particularly
true below \( M_A \approx 120 \text{ GeV} \) (which corresponds to \( M_{H^\pm} \approx 145 \text{ GeV} \), small window in
the upper right corner of Fig. 2), and more for large than for small values of \( \tan \beta \). The
latter aspect is a consequence of the fact that the BR of the charged Higgs boson into
\( \tau \nu_\tau \) pairs is enhanced at \( \tan \beta = 30 \), a value for which the \( cs \) channel is negligible (see
Ref. [3]). An additional contribution comes from graph 2 in Fig. 1a, which involves
Yukawa vertex contributions proportional to \( \tan \beta \). However, the largest part of the
signal cross section is due to graph 1 in Fig. 1a, because of a resonant top decay. The
steep decrease of the signal rates around \( M_A \approx 150 \text{ GeV} \) is due to the opening of the
\( H^\pm \to tb \) off-shell decay channel (see Refs. [3, 22]).

Concerning the background processes (2)–(4), one notices that they are ‘roughly’
independent of \( M_A \) and \( \tan \beta \). This is obvious for processes (3)–(4), as they proceed
through SM graphs (Figs. 1c and d), whereas for process (2) this indicates that the

\[4\]Actually, we have done done so only in the production processes (those represented by the graphs
in Fig. 1a,b,c and d). In fact, for process (5), to describe the decay chain \( t \to bW^\pm \to bjj \), we have used
a Narrow Width Approximation (NWA) for the top, by implementing the decay formulae as given in
Ref. [1]. This has been done in order to avoid a large consume of CPU time in computing exactly a
2 \( \to 6 \) partonic process convoluted with initial structure functions and in presence of multiple resonant
peaks in different regions of the phase space. We are confident that such an approximation does not
spoil the validity of our conclusions.
contributions to the total cross section due to interactions involving MSSM vertices (that is, graphs 8 and 11 in Fig. 1b) are irrelevant (even at $\tan \beta = 30$). We also notice that, unlike processes (2)–(3), reaction (4) is not an irreducible background, as its final state is different from that of the signal. Nevertheless, as it includes two bottom quarks among the produced particles, the probability that its final signature be the same as the signal is (neglecting the misidentification of light flavour quarks as $b$’s as well as correlations between the two possible tags): $P = 1 - B$, where $B = 2\varepsilon_b - \varepsilon_b^2$, $\varepsilon_b$ being the efficiency of tagging one $b$-jet. Hence, better $b$-tagging leads to lower detection rates of the background process (4).

Therefore, from the figure it is clear that in principle a large excess of $\tau$ events could be produced in the scattering process, provided that $M_A < 120 - 130$ GeV (at large $\tan \beta$’s such an interval can be possibly extended up to 130–140 GeV). The possibilities of actually disentangling the signal depend strongly on the detector performances of the LHC, in particular in recognising the displaced vertex in jets which originate from $b$-quarks. In fact, the signature that one would look for is $b\bar{j}\tau\not{E}_T X$, where $\not{E}_T$ represents the missing (transverse) energy due to the neutrino escaping the detectors and $j$ is the jet arising from the light parton scattered in the proton. In order to quantify the significance of the signals we list in Tab. I the total cross sections of processes (1)–(4) (as read from Fig. 2) for $M_A = 60(80)[100]\{120\}$ GeV (corresponding to $M_{H^\pm} = 100(113)[128]\{144\}$ GeV), for both values of $\tan \beta = 1.5$ and 30, multiplied by the $b$-tagging efficiencies and by the yearly luminosity $\int L dt = 10$ fb$^{-1}$ (the minimum considered for the final collider design). Furthermore, we also compute the relative excess of signal events $S$ respect to the total background $B$, as $\Delta = S/B \times 100$. For the microvertex performances, we have adopted the following three reference values: $\varepsilon_b = 1.0, 0.75$ and 0.5. From the numbers given there one deduces that the relative excess of $H^\pm$ events is always quite large, especially at $\tan \beta = 30$, and that the absolute statistics is huge, between $O(10^4 - 10^5)$ signal events per year. In our opinion then, given the expected performances of the LHC detectors, such signals could well be detectable soon after turning on the machine. Moreover, we stress that, as the total luminosity gets larger, the significance of the signal with respect to the total background will increase further.

However, before drawing optimistic conclusions, one has to carefully consider first the kinematic properties of processes (1)–(4), as the LHC detectors will have a finite coverage (for example, in pseudorapidity $\eta$ and transverse momentum $p_T$ of the visible particles). Hence, we have plotted in Figs. 3 and 4, the differential spectra in the above variables for both signal and background processes. If one assumes that the phase space region that can be covered experimentally is approximately the one delimited by the requirements $|\eta(b, \tau, j)| < 3$ and $p_T(b, \tau, j) > 20$ GeV, then one can easily verify that most signal events are contained in the detectable region (we have checked that also in the case $M_A = 60$ GeV one gets distributions similar to those of Fig. 3 and 4). This is true for background events as well, process (4) being possibly the only exception (in the pseudorapidity spectra, upper left corner in Fig. 4a and b). In the end then, one should expect that usual selection criteria will not alter the conclusions that were drawn.

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5 We believe that hadronic $\tau$ decays can be easily distinguished from quark and gluon jets.

6 In first approximation, we assume that the rejection factor for misidentification of light quarks and gluons as $b$-jets is large enough, that we can neglect the reducible QCD background here.
previously extracted from the total rates of Tab. I.

If the charged Higgs mass is above the $t\bar{b}$ threshold, $H^\pm$ scalars could reveal themselves via the production and decay mechanism (5). For a heavy $H^\pm$ boson, we consider then the signature $bbjjjX$, where $b$ represents either a quark or the corresponding antiquark, and $j$ a jet that does not show a displaced vertex. In this case, the final state that should be detected is much more complicated than that of an intermediate mass $H^\pm$ boson, as it is made up of six jets. Nevertheless, the complex resonant structure of process (5) brings some advantages to the tagging procedure. In fact, on the one hand, three vertex tags are now required (which introduce the suppression factor $\varepsilon_3$), and in a high hadronic multiplicity environment; in addition, complications arise from the combinatorics of the the jets. On the other hand, the kinematics of the jets in the final state is highly constrained, since: (i) one of three possible $jj$ combinations must reproduce the $W^\pm$ mass (i.e., $M_{jj} \approx M_{W^\pm}$); (ii) one of the nine possible $bjj$ combinations must reproduce at the same time the $t$ and $W^\pm$ masses (i.e., $M_{bjj} \approx m_t$, with $M_{jj} \approx M_{W^\pm}$). In this respect, note that in the decay chain $t \rightarrow bW^\pm \rightarrow jj$ we do not need to consider intermediate $H^\pm$ contributions, as in the heavy $M_{H^\pm}$ range the $t \rightarrow bH^\pm$ is forbidden.

The total cross section for process (5) is displayed in Fig. 5, as a function of the $A$ mass in the range $140 \text{ GeV} < M_A < 480 \text{ GeV}$ (for both $\tan \beta = 1.5$ and 30). Both the $t \rightarrow bW^\pm$ and $W^\pm \rightarrow jj$ branching ratios are included. For comparison, we also reproduce from Fig. 1 the rates for process (1). A first feature that is worth noticing in Fig. 5 is that again the rates of process (5) for $\tan \beta = 30$ are larger than those for $\tan \beta = 1.5$. In practice, there are two opposite effects which take place: on the one hand, at small $\tan \beta$, the $BR(H^\pm \rightarrow tb)$ is larger whereas, on the other hand, at large $\tan \beta$, the contribution from graph 2 in Fig. 1a is enhanced by couplings proportional to $\tan \beta$ itself. Of the two, it is the second that dominates over most of the $M_{H^\pm}$ range. Furthermore, at large $\tan \beta$'s, processes (1) and (5) yield rates of the same order for $M_A \gtrsim 200$ GeV, such that in this case they can be contemporaneously exploited in searching for $H^\pm$ signals. This is not true at small $\tan \beta$. In general, it should be noted that in Fig. 5 one is dealing with total rates that are more than two orders of magnitude smaller than for the case of an intermediate mass $H^\pm$ boson in the $\tau \nu_\tau$ channel. Nevertheless, as a starting point one can rely on $O(10 - 100)$ signal events produced via $H^\pm \rightarrow tb$ per year (for the same luminosity as above). Clearly, in this case the need for a high value of $\varepsilon_b$ is crucial. For example, a vertex tagging efficiency of 50% reduces the production rates by a factor of 8.

In Fig. 6 we plot the spectrum in the sum of the invariant mass of all possible $bbjj$ combinations entering in process (5). The values of $M_A$ considered here as a reference are 200, 300, 400 and 500 GeV. Since at least one of the $bbjj$ systems is made up by the decay products of the charged Higgs boson, a peak should possibly appear in the distributions (at $M_{H^\pm} = 215, 311, 408$ and 506 GeV, respectively), on top of the combinatorial background. Indeed, the resonant peaks are quite sharp (the $H^\pm$ widths

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7 Also note that at the same time, since $M_{H^\pm} > m_t + m_b$, the first graph in Fig. 1a is no longer resonant.

8 Note that in our NWA approach we automatically obtain $M_{bjj} = m_t$ for the right three jet combination. In the case of the $W^\pm$ decay we have adopted the ‘conservative’ requirement $|M_{jj} - M_{W^\pm}| < 15 \text{ GeV}$.
are approximately, for the above values of mass: 0.84, 3.03, 5.20 and 7.20 GeV at both 
$tan\beta$ values), and clearly visible. However, the total number of events in the region, say, 
$|M_{b\bar{b}} - M_{H^\pm}| < 25$ GeV is, for $tan\beta = 30$: 25(10)[3], 9(4)[1], 4(2)[0.4] and 2(1)[0.2] (for 
the four masses above), for 10 fb$^{-1}$ per year of luminosity, assuming $\varepsilon_b = 1(0.75)[0.5]$. 
Therefore, at least for not too heavy $H^\pm$'s and high $b$-tagging performances, one could 
possibly look for $H^\pm$ signals in the $tb$ channel at large $tan\beta$'s. Certainly, if the high 
luminosity option $\int Ldt = 100$ fb$^{-1}$ can be achieved at the LHC, things would be very 
optimistic, as in a few years of running, even the very heavy mass region could be 
scanned. At small values of $tan\beta$ one has to consider rates that are typically smaller 
by one order of magnitude, rendering Higgs detection much more difficult.

Finally, in Fig. 7, we show the differential spectrum in transverse momentum of 
the various $bbjj$ combinations that can be reconstructed from process (5), for the same 
values of $M_A$ as above. We notice that from the figure it is clear that the $p_T$ spec-
trum of the Higgs decay products is significantly hard (because of the large mass of 
the scalar), a feature that could well help in disentangling heavy $H^\pm$ boson signals, 
especially considering that the ordinary QCD background in six-jet events has quite a 
soft transverse momentum distribution.

4. Conclusions

In this paper we have studied, within the $\mathcal{MSSM}$, a new production mechanism of 
charged Higgs bosons $H^\pm$ at LHC energies, via $b$-quark initiated interactions. Two 
possible Higgs signatures have been considered, depending on whether the mass $M_{H^\pm}$ 
is below or above $m_t + m_b \approx 180$ GeV.

In the first case, by exploiting one vertex tag on one $b$-jet in the final state, the 
Higgs decay channel $H^\pm \rightarrow \tau\nu\tau$ should be identifiable as a clear excess in the number 
of $\tau$ events with respect to the rates predicted by the non-SUSY backgrounds, provided 
that $M_A \lesssim 130$ GeV (i.e., $M_{H^\pm} \lesssim 144$ GeV), both at large and small values of $tan\beta$. 
Also, the absolute number of signal events is statistically very large. In this mass range, 
a careful treatment of various background sources has been performed.

In the second case, the channel $H^\pm \rightarrow tb \rightarrow b\bar{b}jj$ (via hadronic $W^\pm$ decays of the top) 
has been considered. The signature arising from heavy $H^\pm$ decays is complicated (a 
six-jet final state involving three $b$-jets) and only a small number of events is expected. 
Nonetheless, the resonant behaviour of the $t$, $H^\pm$ and $W^\pm$ decay products should allow 
one to eliminate the ordinary QCD background in light quark and gluon jets, although 
in the heavy mass range) a signal-to-background analysis has not been performed. 
In general, if high $b$-tagging performances can be achieved and/or the high luminosity 
option becomes available at the LHC, $H^\pm$ scalars with masses up to 500 GeV could 
well be searched for, as the combinatorial background does not spoil the form of the 
Higgs peaks. This is however true only for large values of $tan\beta$, since for low $tan\beta$'s 
the event rates are smaller by one order of magnitude.

The range between $M_A \approx 130 - 140$ GeV and up to the opening of the $tb$ decay 
threshold is extremely difficult to cover, as rates in the $\tau\nu\tau$ channel drastically decrease 
well below the background rates and at the same time the off-shell $tb$ channel has a 
very small statistics.
Finally, we stress that, before drawing any firm conclusion from our results, one should include a realistic simulation of the expected performances of the LHC detectors and that, in the heavy mass range $M_{H^\pm} > m_t + m_b$, a detailed background study (including all the hadronisation effects in a six-jet final state, an analysis which was beyond our capabilities) should be performed. Nevertheless, we believe that the matter presented here would deserve experimental attention when proceeding to the various simulations of the MSSM Higgs phenomenology at the CERN hadron collider.

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**Appendix**

In this additional section we write down in analytic form the matrix element for the signal processes. As an example, we reproduce that of the reaction $bU \rightarrow bDH^+ \rightarrow bD\tau^+\nu_\tau \oplus C.C.$ However, by replacing $\tau \rightarrow t$ and $\nu_\tau \rightarrow b$ one can easily obtain that for top-bottom (on-shell) production. In fact, we have used a Narrow Width Approximation for the top when this is produced from the $H^\pm$ splitting, by computing the exact amplitude squared for $bU \rightarrow bDH^+ \rightarrow bDtb \oplus C.C.$ and by interfacing this with a SUBROUTINE implementing the top decay formulae into $bW^\pm$ pairs as given in Ref. [19].

The matrix element squared (summed/averaged over the final/initial spins and colours) for the process $bU \rightarrow bDH^+ \rightarrow bD\tau^+\nu_\tau$ reads as:

$$|\mathcal{M}|^2 = |\mathcal{M}_0|^2 P_H^2 P_W^2 (|\mathcal{M}_t|^2 + |\mathcal{M}_\phi|^2 + 2|\mathcal{M}_t^*\mathcal{M}_{\phi}|),$$

with

$$|\mathcal{M}_0|^2 = (g^4 / 2M_W^2) [p_\tau \cdot p_\nu_\tau (m_\tau^2 \tan^2 \beta + m_{\nu_\tau}^2 \cot^2 \beta) - 2m_\tau^2 m_{\nu_\tau}^2]$$

$$P_H = (p_H^2 - M_H^2 + iM_H\Gamma_H)^{-1}$$

$$P_W = (p_W^2 - M_W^2 + iM_W\Gamma_W)^{-1}$$

$$|\mathcal{M}_t|^2 = 2|P_t|^2 p_{b,in} \cdot p_U \times$$

$$\times [2m_b^2(m_t^2 + p_{b,out} \cdot p_t \tan^2 \beta) p_t \cdot p_D + (m_t^4 \cot^2 \beta - m_b^2 p_t^2 \tan^2 \beta) p_{b,out} \cdot p_D]$$

$$|\mathcal{M}_\phi|^2 = m_b^2 \sec^2 \beta (2p_H \cdot P_D p_H \cdot p_U - p_H^2 p_U \cdot p_D) \times$$

$$\times [m_b^2(|P_{H_0,h0}^2| - |P_{A_0}|^2) + p_{b,out} \cdot p_{b,in} (|P_{H_0,h0}|^2 + |P_{A_0}|^2)]$$

$$2|\mathcal{M}_t^*\mathcal{M}_\phi| = m_b^2 \sec \beta \times$$

$$\times [\Re[P_t^*(P_{H_0,h0} - P_{A_0})] m_b^2 \cot \beta - \Re[P_t^*(P_{H_0,h0} + P_{A_0})] m_b^2 \tan \beta] \times$$

$$\times (p_{b,out} \cdot P_D P_H \cdot p_U + p_{b,out} \cdot p_U P_H \cdot P_D - p_{b,out} \cdot P_H P_U \cdot P_D).$$
where

\[ p \]

Here we have set \( m \) of a complex number, respectively, and that \( \epsilon \)

\[ \Re \]

initial/final state). Note that the symbols \( \Re \) and \( \Im \) refer to the real and imaginary part of a complex number, respectively, and that \( \epsilon_{\mu\nu\lambda\sigma} \) is the Levi-Civita tensor \( (\epsilon_{0123} = 1) \).

Finally, by exchanging \( \rho_{b,\text{in}} \leftrightarrow -\rho_{b,\text{out}} \) and \( \epsilon_{\mu\nu\lambda\sigma} \leftrightarrow -\epsilon_{\mu\nu\lambda\sigma} \) one can obtain the amplitude squared for \( bU \) fusion, and by relabelling \( U \leftrightarrow D \) those for the \( bD \)- and \( bD \)-initiated reactions.

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Table Captions

[I] Number of events for signal (1) and total background (2)–(4), at the LHC with CM energy $\sqrt{s}_{pp} = 14$ TeV, for $M_A = 60(80)[100]\{120\}$ GeV and $\tan \beta = 1.5$ and 30, assuming the yearly luminosity $\int \mathcal{L} dt = 10$ fb$^{-1}$ and the $b$-tagging efficiencies $\varepsilon_b = 1.0, 0.75$ and 0.5 (first, second and third row, respectively), together with the relative excess of signal events respect to the total background.
Figure Captions

[1] Feynman diagrams contributing at lowest order to the subprocess $bU \to bD\tau^+\nu_\tau \oplus C.C.$: (a) via $H^\pm$ resonant graphs; (b) via $W^\pm$ resonant graphs and through EW only; (c) via $W^\pm$ resonant graphs and through QCD interactions; and to the subprocess $UD \to b\bar{b}\tau^+\nu_\tau \oplus C.C.$: (d) via $W^\pm$ resonant graphs and through QCD interactions. Here, $U$ and $D$ represent any of the light quarks $u, d, s$ and $c$. The PostScript version of the Feynman graphs has been produced using MadGraph.

[2] Cross section of the four processes (1)–(4), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, in the region $60$ GeV $\lesssim M_A \lesssim 480$ GeV and for two different values of $\tan\beta$ (in the case of processes (1) and (2)). In the top left hand plot we enlarge the region $60$ GeV $\lesssim M_A \lesssim 150$ GeV. Solid line: process (1) with $\tan\beta = 1.5$. Dashed line (large spacing): process (1) with $\tan\beta = 30$. Dotted line (large spacing): process (2) with $\tan\beta = 1.5$. Dot-dashed line: process (2) with $\tan\beta = 30$. Dashed line (small spacing): process (3). Dotted line (small spacing): process (4). The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, except for neutrinos. The structure function set MRSA has been used.

[3] Differential distribution in transverse momentum of the $b$-quark (a) and of the $\tau$-lepton (b) for the four processes (1)–(4), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, for the following selection of masses $M_A = 80, 100, 120$ GeV and for two different values of $\tan\beta$ (in the case of processes (1) and (2)). Solid line: process (1) with $\tan\beta = 1.5$. Dashed line (large spacing): process (1) with $\tan\beta = 30$. Dotted line (large spacing): process (2) with $\tan\beta = 1.5$. Dot-dashed line: process (2) with $\tan\beta = 30$. Dashed line (small spacing): process (3). Dotted line (small spacing): process (4). Please note that the two curves corresponding to process (2) are practically indistinguishable. The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, except for neutrinos. The structure function set MRSA has been used.

[4] Differential distribution in pseudorapidity of the $b$-quark (a) and of the $\tau$-lepton (b) for the four processes (1)–(4), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, for the following selection of masses $M_A = 80, 100, 120$ GeV and for two different values of $\tan\beta$ (in the case of processes (1) and (2)). Solid line: process (1) with $\tan\beta = 1.5$. Dashed line (large spacing): process (1) with $\tan\beta = 30$. Dotted line (large spacing): process (2) with $\tan\beta = 1.5$. Dot-dashed line: process (2) with $\tan\beta = 30$. Dashed line (small spacing): process (3). Dotted line (small spacing): process (4). Please note that the two curves corresponding to process (2) are practically indistinguishable. The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, except for neutrinos. The structure function set MRSA has been used.

[5] Cross section of processes (1) and (5), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, in the region $140$ GeV $\lesssim M_A \lesssim 480$ GeV and for two different values of $\tan\beta$. Solid line: process (1) with $\tan\beta = 1.5$. Dashed line (large spacing): process (1) with $\tan\beta = 30$. Dashed line (small spacing): process (5) with $\tan\beta = 1.5$. Dotted
line: process (5) with $\tan \beta = 30$. The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, including the top decay products. The structure function set MRSA has been used.

[6] Differential distribution in invariant mass of the $b\bar{b}jj$ systems for process (5), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, for the following selection of masses $M_A = 200, 300, 400, 500$ GeV, for $\tan \beta = 1.5$ (solid line) and 30 (dashed line). The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, including the top decay products. Bins are 5 GeV wide. The structure function set MRSA has been used.

[7] Differential distribution in transverse momentum of the $b\bar{b}jj$ systems for process (5), at the LHC for $\sqrt{s}_{pp} = 14$ TeV, for the following selection of masses $M_A = 200, 300, 400, 500$ GeV, for $\tan \beta = 1.5$ (solid line) and 30 (dashed line). The cut $p_T^{\text{final}} > 10$ GeV has been applied to all particles in the final states, including the top decay products. The structure function set MRSA has been used.
$N_{ev}(b\tau E_T^X)$

| $S$       | $B$                  | $\Delta$ |
|-----------|----------------------|----------|
| 386(289)[170]{62} $\times 10^3$ | 630(645)[654]{671} $\times 10^3$ | 61(45)[26]{9}% |
| 289(217)[127]{47} $\times 10^3$ | 488(498)[506]{518} $\times 10^3$ | 59(44)[25]{9}% |
| 193(145)[85]{31} $\times 10^3$  | 375(383)[387]{396} $\times 10^3$ | 51(38)[22]{8}% |

$\tan \beta = 1.5$

| $S$       | $B$                  | $\Delta$ |
|-----------|----------------------|----------|
| 551(436)[294]{145} $\times 10^3$ | 623(639)[651]{672} $\times 10^3$ | 88(68)[45]{22}% |
| 413(327)[220]{109} $\times 10^3$ | 483(494)[504]{519} $\times 10^3$ | 86(66)[44]{21}% |
| 275(218)[147]{73} $\times 10^3$  | 372(380)[386]{396} $\times 10^3$ | 74(57)[38]{18}% |

$\tan \beta = 30$

$M_A = 60(80)[100]{120}$ GeV

$p_T^{\text{final}} > 10$ GeV

$\sqrt{s_{pp}} = 14$ TeV

$\int \mathcal{L} dt = 10$ fb$^{-1}$

Tab. I
Fig. 1c
Fig. 1d
Fig. 6
Fig. 2.