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Abstract: Double recalescence in many ferrous alloy systems involves rapid solidification of metastable ferrite from the undercooled melt with subsequent transformation to stable austenite. Containerless processing is used to monitor the process using pyrometry and high-speed cinematography such that delay behavior can be predicted based on the application of the retained damage model (RDM). When comparing Fe-Cr-Ni alloys to Fe-Co alloys, the cluster attachment rate is enhanced while free energy retention is reduced. These trends are tied to specific alloy properties. A retained free energy criterion is proposed based on the ratio of thermophysical properties used to define the transformation driving force such that the thermodynamic limit for energy retention may be predicted. Surprisingly, at long delay times, healing occurs such that much of the retained free energy is not available to enhance the transition from metastable to stable phases. At delay times less than one second, no healing is observed and the RDM correctly predicts transformation delay behavior over a wide range of alloy compositions.

Keywords: nonclassical nucleation; rapid solidification; double recalescence; undercooling

1. Introduction

In order to control the phase selection and subsequent microstructural evolution in solidification processes involving rapid heat extraction, such as additive manufacturing, spray forming, and welding, the thermodynamic limits that define transformation kinetics must be understood. The retained damage model (RDM) is used to predict the delay, or incubation time, between primary and secondary recalescence events during rapid solidification, where transformation from molten metallic alloy liquid passes through a metastable intermediary primary phase before conversion to a stable secondary phase. The RDM was developed to explain the influence of undercooling and stirring on the conversion of metastable bcc ferrite to stable fcc austenite in ternary Fe-Cr-Ni alloys [1–8]. Previous work showed that the influence of undercooling alone may be evaluated by investigation of transformation behavior during processing using electrostatic levitation (ESL), where convection during undercooling is negligible. This contrasts the behavior during electromagnetic levitation (EML) processing where convection and undercooling simultaneously impact the delay. By applying the results from ESL to the EML results, it is possible to isolate the impact on transformation delay due to convection alone. No previous modeling effort has successfully been employed to numerically distinguish between these effects.

The model is based on an analogy of hot working of a material whereby defect energy is introduced into a microstructure to drive subsequent recrystallization to the parent phase (known as healing) or promote transformation to a new phase. In the case of the Fe-Cr-Ni alloy family, the introduction of this damage free energy results in significant reduction in the delay time observed between the primary and secondary nucleation events in a process known as double recalescence.
The model relies on an evaluation of the global thermodynamic limit to how much free energy can be retained to subsequently drive the second transformation [1]. In addition to the classical free energy contribution resulting from undercooling relative to the stable phase $\Delta G_s$ [6], when defining the total free energy that drives the transformation $\Delta G_T$, as seen in Equation (1), a second and third term are added to track the contribution from metastable undercooling $\Delta G_m$ and melt shear $\Delta G_c$; in the absence of convection, this third term goes to zero. These terms may be reduced by healing, and this effect is tracked using an experimentally derived retained energy parameter $f_x$, representing the fraction of available free energy from primary undercooling, which is retained:

$$\Delta G_T = \Delta G_s + \Delta G_m + \Delta G_c \Delta G_e = \frac{\Delta T_s}{T_{ls}} \frac{\Delta H_s}{\Omega_s} \quad \Delta G_m = f_x \frac{\Delta T_m}{T_{lm}} \frac{\Delta H_m}{\Omega_m} \quad \Delta G_c = 0 \quad (1)$$

The relationship between delay time and free energy is based on the principle of microscopic reversibility [7] such that, in a manner functionally constant with Kantrowicz [8] and Kaschiev [9], the delay is inversely proportional to the attachment rate $\beta$ and the free energy raised to the fourth power, $m = 4$ [1], as shown in Equation (2). $\beta$ represents a measure of the success rate for an atom attaching to the cluster as it grows to critical size. Note that the negative sign in the original derivation is required since the curvature at critical size is negative.

$$\tau = -\frac{\kappa k_B T}{2 f_x \Delta G_m} = \frac{128 \pi k_B T \gamma^3 f(\theta)}{\beta \Delta G_m^4} \left( \frac{N_A}{\Omega} \right) \quad (2)$$

A dimensionless approach is then used to evaluate model performance using a reference state representing the longest delay time possible, which occurs at the minimum free energy condition, as seen in Equation (3). This reference state is defined from the equilibrium phase diagram, where $\Delta T_m = 0$, $\Delta G_m = 0$, and $\Delta G_R = \Delta G_c$. The dimensionless driving force $N_M$ is based on the ratio of the total free energy at the conditions where the experiment was run, including any retained energy, to the free energy at the reference state. Thus, $N_M$ is only a function of the experimentally observed undercooling $\Delta T_m$ from Equation (1). The dimensionless delay time $N_D$ is based on the ratio of the corresponding experimentally observed delay time to the delay at the reference state, as calculated using Equation (2). Since the undercooling (measured using pyrometry) and delay time (measured using high-speed cinematography) are independently evaluated during any given experiment, these two dimensionless quantities are independent of each other.

$$N_M = \frac{\Delta G_T}{\Delta G_R} \quad N_D = \frac{\tau}{\tau_R} \quad (3)$$

The treatment shown in Equation (1) defines a third dimensionless quantity $N_\Xi$, shown in Equation (4), representing the ratio of thermophysical properties for metastable and stable phases such that the thermodynamic limit representing the maximum value of $f_x$ is defined. Refer to Appendix A for derivation and application of these relationships.

$$N_\Xi = \frac{\Delta H_m / T_{lm}}{\Delta H_s / T_{ls}} \frac{\Omega_m}{\Omega_s} \quad (4)$$

It is expected that the attachment frequency $\beta$ is higher for Fe-Co than for Fe-Cr-Ni [10] for two reasons: First, the liquidus temperatures for Fe-Co alloys are substantially higher than for steel and attachment is assumed to be a thermally-activated process. Second, since the partitioning coefficient shown in Figure 1a is closer to one for Fe-Co, the cluster and parent phase compositions are similar, thus reducing the solute compositional barrier for a stable-phase cluster formation. Conversely, the fraction of damage energy retained $f_x$ should be lower because $N_\Xi$ is lower, as seen in Figure 1b. This is because $N_\Xi$ and $f_x$ are each proportional to the ratio of the free energy required from the metastable phase to that
available to the stable phase; refer to Appendix A for the derivation of the criterion limiting \( f_x \leq N_\Xi \). For Fe-Cr-Ni, \( f_x \to 1 \) as \( N_\Xi \to 1 \) and we expect that for Fe-Co, since \( N_\Xi < 1 \) and \( f_x < 1 \). The purpose of this paper is to investigate these hypotheses in an effort to apply the retained damage model to a new alloy system [10–13].

![Figure 1](image_url)

**Figure 1.** Characterizing key physical properties from Fe-Co and Fe-Cr-Ni alloy systems. (a) Dimensionless partitioning coefficient \( k = C_\Xi/C_\Lambda \) for metastable (m) and stable (s) solid phases; for FeCrNi, the metastable bcc phase rejects Ni and the stable fcc phase rejects Cr; for FeCo, both metastable and stable phases reject the solute Co; (b) dimensionless property parameter \( N_\Xi \).

### 2. Materials and Methods

#### 2.1. Containerless Processing Using Electrostatic Levitation

Fe–Co samples were prepared at three compositions of 30, 40, and 50 at % cobalt from pure elemental stock with 99.995% pure Fe and 99.95% pure Co. The components were arc-melted under an argon atmosphere such that the spherical samples had a mass of approximately 40–60 mg (~2 mm diameter). Negatively charged samples were inserted into the NASA Marshall Space Flight Center ESL and levitation was achieved by applying a negative charge to the lower electrode and a positive charge to the upper electrode within a vacuum chamber evacuated to an atmosphere of \( 10^{-9} \) mbar. The location of the sample was determined by positioning lasers such that the lateral and vertical position could be adjusted by PID control. The sample was melted using a 200 watt continuous wave Nd:YAG laser, and then the molten spherical droplet was allowed to radiatively cool until solidified [14]. Containerless processing of these alloys ensures that contamination of the melt by crucible walls is minimized to encourage attainment of deep undercooling. Since we evaluated data obtain from experiments run using NASA ESL, induced convection was minimized, and any stirring produced by Marangoni convection, resulting from thermal gradients imposed during melting, was dampened out to produce a quiescent melt [15,16].

#### 2.2. Process Monitoring

During the entire heating cycle, the thermal profile was monitored with a Mikron Infrared Inc. Mi-GA140 single color pyrometer, operating at 16 Hz, with a wavelength range from 1.45 to 1.8 µm, and calibrated using a Mikron M390 blackbody generator, (Integrated Component Sales, Winter Park, FL, USA) [17]. Directly before primary recalescence and continuing throughout the solidification process, nucleation and growth were monitored with a high-speed digital camera with frame capture rates of up to 50,000 frames per
second. The camera was selected based on the temporal and spatial resolution desired for a particular test series and depended on the sample radiance for a given alloy and undercooling range. There were three cameras that were used during testing: Vision Research Phantom V7.1 (Vision Research, Wayne NJ, USA), Integrated Design Tools - IDT MotionPro Y4, and IDT MotionPro Y7 (DEL Imaging Systems LLC, Cheshire CT, USA) [18]. Image contrast during recalescence is developed based on the differences in radiative intensity associated with the temperature of each phase present; undercooled liquid is dark, the metastable mushy zone is brighter, and the stable phase is brightest. During recalescence, it is possible to track the motion of the growth interface across the sample and thus define the time and location of any nucleation event.

Representative examples of these two methods to evaluate the delay are shown in Figure 2, where four key events are annotated as (1) undercooled liquid, (2) nucleation and growth of the primary metastable phase, (3) mushy zone isothermal hold at the metastable liquidus, and (4) nucleation and growth of the stable phase with recalescence to the stable phase liquidus. The bright spots on the sample are introduced by reflection from the ESL positioning laser system.

![Figure 2. Double recalescence. (a) Thermal profile from Fe70Co30 pyrometry with annotation of timing of key events; (b) mosaic of Fe60Co40 images showing ① undercooled liquid, ② growth of metastable primary phase, ③ isothermal metastable phase mushy zone delay, and ④ growth of secondary stable phase.](image)

2.3. Analysis Methods

The analytical approach used involved selecting a cluster geometry and attachment mechanism, as previously described in earlier RDM publications [1,2]. As the total metastable phase undercooling approaches zero, the value of $\Delta G_T$ approaches the reference condition $\Delta G_R$ and the delay $\tau$ is supposed to approach $\tau_R$. Under these conditions $N_M$ and $N_D$ approach 1 and the experimentally derived values at the correct value of $\beta$ will converge to intersect the axes of a log-log plot at the origin. This defines the attachment rate.

Once the attachment rate is known, experimental values of $\tau$ are used to estimate the quantity of retained free energy that is required to obtain the observed delay using Equation (2). This value is compared to an estimate of the retained free energy $\Delta G_M$ available as calculated from the observed undercooling using Equation (1). A plot of these two quantities yields the slope $f_\tau$, which must be less than $N_S$, based on the retained free energy criterion developed in Appendix A.

3. Results

A plot of the experimentally observed delay times is shown as a function of the undercooling relative to the stable phase in Figure 3. The three alloys studied are differentiated...
by symbol color. For example, the Fe$_{60}$Co$_{40}$ (at %) alloy is named 60-40 and displayed in yellow. Note that the low undercooling (long delay time, red points) behavior for the 70-30 alloy differs significantly from that at high undercooling (short delay time, green points). Since the RDM predictions indicate that the delay time is inversely proportional to the attachment rate, if we increase $\beta$, all the solid lines representing model predictions will move down. All lines move together since we assume a common value of $\beta$ for the entire alloy family; thus, it is easy to identify the appropriate attachment rate from experimental data by minimizing the variance between observed and predicted values for each test. The best fit is obtained for a value of $\beta = 2 \times 10^8$ atoms/s.

![Graph showing delay time as a function of undercooling](image)

**Figure 3.** Experimentally observed delay time as a function of undercooling ($\Delta T = \Delta T_s + \Delta T_m$) for the three alloys studied with RDM predictions of behavior, assuming an attachment rate of $\beta = 2 \times 10^8$ atoms/s.

A comparison of the Required $\Delta G_m$ from the measured delay times with the Available $\Delta G_m$ from the measured undercooling results in a slope of $f_x = 0.410 \pm 0.022$ for tests with delay times shorter than one second, shown in Figure 4a, and $f_x^{\text{heal}} = 0.0753 \pm 0.0052$ for long delay times (only the 70-30 alloy showed healing), displayed in Figure 4b. In subsequent calculations, values of 0.40 and 0.075 are used.
**4. Discussion**

The discussion section is provided in four parts to highlight the influence of key experimentally determined parameters on the performance of the RDM. A summary of the key parameters used in the calculations to define the RDM predictions is provided in Table 1. If two values are presented, the first is for the metastable bcc ferrite, while the second is for the stable fcc austenite phase. Where appropriate, literature references are indicated in the units column of Table 1.

**Table 1. Retained damage model parameters.**

| Parameter | Units | 70-30 Heal | 70-30 | 60-40 | 50-50 |
|-----------|-------|------------|-------|-------|-------|
| $T_L$     | K     | 1753/1763  | 1753/1763 | 1733/1757 | 1714/1754 |
| $\Delta H$ | J/mol | 10,999/14,098 | 10,999/14,098 | 10,767/14,083 | 10,795/14,154 |
| $\Omega$  | m$^3$/mol | $7.46 \times 10^{-6}$ | $7.46 \times 10^{-6}$ | $7.40 \times 10^{-6}$ | $7.33 \times 10^{-6}$ |
| $k$       | -     | 0.949/0.977 | 0.949/0.977 | 0.960/0.989 | 0.969/0.997 |
| $N_{\Sigma}$ | -     | 0.785 | 0.785 | 0.775 | 0.780 |
| $\Delta T_{\sigma/m}$ | - | K | 13 | 10 | 24 | 40 |
| $C$       | atom$^3$·m$^{-12}$ | $3.91 \times 10^{37}$ | $3.92 \times 10^{37}$ | $3.94 \times 10^{37}$ | $3.96 \times 10^{37}$ |
| $\Delta G_R$ | J/m$^3$ | $1.39 \times 10^{7}$ | $1.07 \times 10^{7}$ | $2.60 \times 10^{7}$ | $4.40 \times 10^{7}$ |
| $\tau_R$ | s     | 5.18 | 14.82 | 0.430 | 0.053 |

**4.1. Attachment Rate $\beta$**

The attachment rate is a measure of the success rate of the incremental growth of the subcritical cluster, and we expected that several material properties would influence the value of this quantity. Since attachment is probably a thermally activated process akin to diffusion, the metastable liquidus temperature is an important parameter because this represents the isothermal hold temperature that characterizes conditions during which the stable cluster develops. The alloys studied have a liquidus in the range of $1669 < T_{Lm}^{FeCrNi} < 1716$ K [1,2] for the steels and $1714 < T_{Lm}^{FeCo} < 1753$ K [11,13] for Fe-Co; thus, we expected attachment to be greater for Fe-Co based on an anticipated increase in attachment attempt frequency. Additionally, differences in solute concentration between the parent phase and the developing critical nucleus tend to present a barrier to cluster growth. As the partitioning coefficient approaches one, the attachment/detachment process will become more reversible. Partitioning for the stable phase is more significant for steels with $k^{FeCrNi} \approx 0.75$ than for Fe-Co with $k^{FeCo}_{stable} \approx 0.98$, indicated in Figure 1a. Again, we expected the attachment rate to be greater for Fe-Co based on an anticipated increase in the rate of
attachment success (alternately known as the “accommodation coefficient for growth” [8]). Contrasting attachment rates, the stainless steel value of \( \beta_{\text{FeCrNi}} = 4 \times 10^7 \) atoms/s [1] compares well to the Fe-Co alloy family value, which is on the order of \( 5 \times 10^8 \) atoms/s. Future work will involve investigating if attachment can be linked directly to an Arrhenius-type relationship within an alloy family instead of assuming it is constant for the entire family.

4.2. Retained Energy Parameter \( f_x \)

The retained energy parameter is a measure of the fraction of available free energy from primary undercooling, which is used to promote stable phase nucleation and thus reduce the transformation delay. Key thermophysical properties are combined to develop the properties dimensionless quantity \( N_\Xi \), as shown in Figure 1b. For steels, the parameter \( N_\Xi \to 1 \) implies that all retained free energy is available to drive the transformation; free energy is apparently conserved. This is a seductive argument, but for Fe-Co, the situation is different because \( N_\Xi \) is significantly reduced; based on the retained free energy criterion in Appendix A, the thermodynamic limit requires that \( f_x \) is significantly depressed. Since \( f_x \ll N_\Xi \), the ratio decreases by almost a factor of two, since 0.41 \( \ll \) 0.79. Only half of the free energy available is used. Further work is required to understand the processes behind this observation, but this theory establishes limits that are consistent with behavior across several alloy families.

4.3. Healing at Long Delay Times

An additional attribute of the RDM is the ability to investigate recrystallization of the parent phase during the isothermal hold, which characterizes the delay period; this represents healing of the retained damage. If healing occurs in a particular undercooling range, particularly at long times associated with low undercooling, then it would be expected that the slope would decrease such that it deviates from \( N_\Xi \) dramatically. This was observed for the 70-30 alloy, as shown when comparing the behavior at high undercoolings in Figure 4a (green symbols) with low undercoolings in Figure 4b (red symbols). Special treatment is required to evaluate samples where healing occurs. As seen in Figure 2a, after a brief isothermal hold at the metastable liquidus \( T_{Lm} \), the temperature begins to drop as heat extraction to the environment allows the system to equilibrate to the metastable solidus \( T_{Sm} \). The thermal driving force \( \Delta T_s \) is thus increased such that the solidus temperature replaces the liquidus temperature wherever it appears in Equation (1). This also increases \( \Delta G_0 \) and \( \Delta G_T \) in Equation (1) and \( N_\Xi \) in Equation (4). With a decrease in \( T \) and an increase in \( (\Delta G_T)^m \) in Equation (2), \( \tau_R \) becomes reduced while \( \Delta G_R \) becomes increased; both these significant changes have a substantial effect on the fit in Figure 4b that identifies the slope that defines the healed retained energy parameter \( f_x^{\text{heal}} \ll f_x \).

4.4. Dimensionless Presentation of RDM Predictions

With RDM fit parameters \( \beta = 2 \times 10^8 \) atoms/s, \( f_x = 0.40 \), and \( f_x^{\text{heal}} = 0.075 \), Equation (1) was used to evaluate \( \Delta G_T \) and thus to predict values for \( \tau \) using Equation (2). The results are displayed in Figure 3. The two independent dimensionless parameters may now be calculated using Equation (3). The relationship between these independent variables is plotted in Figure 5, which shows a slope of negative \( m = 3.938 \pm 0.123 \), which agrees well with the theoretical value for a slope of negative \( m = 4 \) from \( \tau = C/\beta(\Delta G_T)^m \), given that the value of \( C \) varies by alloy as shown in Equation (2) and Table 1. Note that for the healed data, there is also agreement is with \( m = 4.042 \pm 0.273 \) based on the proposed modification of the thermal driving force and \( f_x \).
Figure 5. Relationship between dimensionless delay and driving force.

5. Conclusions

The retained damage model, developed for Fe-Cr-Ni rapid solidification, was successfully applied to the Fe-Co alloy family. The results confirmed the hypothesis that the attachment frequency $\beta$ is significantly higher in Fe-Co than observed in Fe-Cr-Ni. Additionally, as predicted, the fraction of available energy that is retained $f_x$ was found to be significantly lower, although the observed value is a factor of two lower than the theoretical maximum predicted by $N_\Xi$, using the retained free energy criterion. A surprising result was the observation of significant healing for delay times longer than one second, a condition only seen for the 70-30 alloy, such that the fraction of available energy at low undercoolings is dramatically reduced; at low undercoolings, $f_x$ starts at a value of 0.075, and when high undercoolings and short delay times are reached for $\tau < 1$ s, this value rises to 0.4, as observed for the rest of the Fe-Co alloy family. No healing appears to be possible if the delay is short enough. Now that the influence of undercooling on transformation delay for FeCo has been defined from ESL tests, future evaluations on the influence of convection on delay may begin based on additional EML testing.

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Appendix A

One key model parameter is the retained energy parameter \( f_x \), which represents the ratio of the retained free energy required to drive the transformation to that available from thermal undercooling. Since there cannot be more free energy retained than was available during primary recalescence, a limit exists on the value of this parameter. In order to numerically define the thermodynamic limits on \( f_x \), the driving force during double recalescence \( \Delta G_T \) must be evaluated based on the relative undercoolings for each transformation, as shown previously in Equation (1). Additionally, we defined a dimensionless property number \( N_\Xi \) in Equation (4) based on the ratio of thermophysical quantities used to define the free energies for each transformation (note that this definition corrects a typographical error contained in [1,2]). Expanding Equation (1) based on Equation (4) yields an expression for the driving force as a function of a modified undercooling term \( \Delta T_T^X \), which transforms contributions by metastable phase free energy terms to a stable phase basis:

\[
\Delta G_T = \Delta G_s + \Delta G_m = \left( \frac{T_s - T_m}{T_s} \right) \left( \frac{\Delta H_s}{T_s} \Omega_s \right) + \left\{ \frac{f_x}{N_\Xi} \right\} \left( \frac{T_m - T}{T_m} \right) \left( \frac{\Delta H_m}{T_m} \Omega_m \right) = \left[ \frac{\Delta H_s}{T_s} \Omega_s \right] \left( T_s - 1 \right) + \left\{ \frac{f_x}{N_\Xi} \right\} \left( \frac{T_m - T}{T_m} \right) \left( \frac{\Delta H_m}{T_m} \Omega_m \right) \quad (A1)
\]

A criterion can thus be developed based on the overall undercooling relative to the stable phase liquidus (equivalent to recalescence from the undercooled liquid directly to the stable phase liquidus \( \Delta T_T \)):

\[
\Delta T_T = \Delta T_s + \Delta T_m = (T_{LS} - T) \quad (A2)
\]

The overall available thermal driving force is thermodynamically limited by the phase diagram such that the function in parentheses from Equation (A1) cannot be greater than the overall undercooling in Equation (A2) and thus \( \Delta T_T^X \leq \Delta T_T \):

\[
\left( T_{LS} + \left\{ \frac{f_x}{N_\Xi} \right\} \left( T_m - T \right) \right) \leq (T_{LS} - T) \quad \left\{ \frac{f_x}{N_\Xi} \right\} \leq 1 \quad (A3)
\]

The retained free energy criterion can therefore be restated as \( f_x \leq N_\Xi \) in the absence of convection. At the extremes, if \( f_x = N_\Xi \), then the two values in parentheses in Equation (4) are equivalent and all free energy is retained such that the thermal driving force corresponds to \( \Delta T_T \). At the other extreme, if \( f_x = 0 \), then there is no contribution by retained energy from primary metastable recalescence and \( \Delta G_T = \Delta G_c \). Note that this new insight requires the original definition of the contribution to free energy from melt convection, or more correctly, from melt shear, be slightly altered as presented in Equation (A4) to account for values of \( N_\Xi \) varying from one such that:

\[
\Delta G_c = \frac{f_x}{N_\Xi} \Delta m \dot{\gamma} \left[ \frac{\Delta \gamma}{\Delta m} - \ln(\dot{\gamma}) \right] \quad (A4)
\]

The inclusion of the dimensionless property number is required because for steel alloys \( N_\Xi^{FeCrNi} \rightarrow 1 \), and this term is ignored. For Fe-Co, \( N_\Xi^{FeCo} \ll 1 \), and it cannot be ignored.

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