New insights into the evolution of the FR I radio galaxy 3C 270 (NGC 4261) from VLA and GMRT radio observations

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ABSTRACT

We present Giant Metrewave Radio Telescope (GMRT) 240 MHz observations of the nearby luminous FR I radio source 3C 270, in the group-central elliptical NGC 4261. Combining these data with reprocessed Very Large Array (VLA) 1.55 and 4.8 GHz observations, we produce spectral index maps that reveal a constant spectral index along the jets and a gradual steepening from the ends of the jets through the lobes towards the nucleus. A Jaffe & Perola (JP) model fitted to the integrated spectrum of the source gives an asymptotic low-frequency index of $\alpha_{\text{inj}} = 0.53^{+0.01}_{-0.02}$. While JP models fitted to the observed spectral index trend along the lobes allow us to estimate radiative ages of $\sim 29$ Myr and $\sim 37$ Myr for the west and east lobes respectively. Our age estimates are a factor of two lower than the 75-Myr upper limit derived from X-ray data (O’Sullivan et al. 2011). We find unlikely the scenario of an early supersonic phase in which the lobe expanded into the ISM at approximately Mach 6 (3500 km s$^{-1}$), and suggest that either the source underwent multiple AGN outbursts with possible large changes in jet power, or possibly that the source age that we find is due to a backflow that transports young electrons from the jet tips through the lobes toward the nucleus relatively quickly. We calculate that in the lobes the energy ratio of non-radiating to radiating particles is $\sim 4 - 24$ indicating significant gas entrainment. If the lobes are in pressure balance with their surroundings, the total energy required to heat the entrained material is $10^{58}$ erg, $\sim 40\%$ of the total enthalpy of the lobes.

Key words: galaxies: groups: general – ageing, radio galaxies: individual (3C 270, NGC 4261) - galaxies: active

1 INTRODUCTION

The study of radio galaxies has become increasingly important as they appear to be natural laboratories uniquely suited to the study of one of the most energetic phenomena in the Universe: relativistic jets arising from the associated active galactic nuclei (AGN). The reason this phenomenon is so important is that radio-loud activity of the central AGN is now considered to be the most likely source of the heating mechanism injecting energy into the hot gaseous halos of groups and clusters of galaxies, thereby balancing the effects of radiative cooling (Fabian 2012, McNamara & Nulsen 2007, Peterson & Fabian 2006).

The evolution of radio galaxies is commonly accepted to pass through three phases (as described in, e.g., Kraft et al. 2007). In the beginning, the inflation of the lobes surrounding the jets is highly supersonic as the lobes appear to be significantly over-pressured in relation to the ambient medium. After this early, most sources short-lived, supersonic phase, the expansion of the lobes continues and their internal pressure drops, approaching equilibrium with the ambient gas. In the final phase jets shut down and the lobes eventually become unobservable due to energy losses. Examples of the complex interactions between radio lobes and a surrounding intra-
Jets and found values of ∼(2013) examined the 1.4-4.8 GHz spectral index of the base of the orthogonal to the radio jets (Tremblay et al. 2009). Laing & Bridle ionization nuclear emission-line region (Ho, Filippenko & Sargent (IGM) (Worrall et al. 2010). The jets emanate from a compact radio core coincident with the optical nucleus of the galaxy (Jones & Wehrle 1997), where optical spectroscopy has revealed a low-ionization nuclear emission-line region (Ho, Filippenko & Sargent 1997). In addition, a nearly edge-on nuclear disk (100-pc-scale) rich in dust, molecular and atomic gas (Jaffe et al. 1993), lies orthogonal to the radio jets (Tremblay et al. 2009). Laing & Bridle (2013) examined the 1.4-4.8 GHz spectral index of the base of the jets and found values of ∼0.65 at ∼14″ from the nucleus, jumping to 0.72 at ∼14″ and then declining to ∼0.6-0.65 at 50″. The spectral index is defined as $S_\nu \propto \nu^{-\alpha}$, where $S_\nu$ is the flux density at the frequency $\nu$.

In the X-ray band, ROSAT images of the NGC 4261 group show diffuse thermal emission and a non-thermal nuclear component at low energies (Worrall & Birkinshaw 1994). Chandra observations reveal X-ray jets in the inner few kiloparsecs of the radio jets (Gliozzi, Sambruna & Brandt 2003; Zezas et al. 2005) and suggest a synchrotron origin for the jet X-ray emission.

More recent analysis of the Chandra and XMM-Newton data in O’Sullivan et al. (2011) shows much structure in the gas in which the galaxy is embedded. The AGN jets have inflated two lobes, producing cavities in the IGM and building up rims of compressed hot gas which almost entirely enclose the lobes. The cavity rims consist of material that has been swept up and compressed by the expansion of the lobes, weakly heated by compression with no evidence of shock heating (O’Sullivan et al. 2011). NGC 4261 hosts a small cool core with radius $\sim 10$ kpc and a temperature of $\sim 0.6$ keV, with the IGM temperature in the group being $\sim 1.6$ keV (Humphrey et al. 2009). The structure of the core has been disturbed by the expansion of the radio lobes and is not spherically symmetric (O’Sullivan et al. 2011), with wedge-shaped surface-brightness decrements that suggest the jets have driven out the IGM (or galactic gas) from conical regions around their first few kiloparsecs (Worrall et al. 2010).

Evidence of anisotropy in the globular cluster distribution has been seen (Giordano et al. 2005; Bonfim et al. 2012; D’Abrusco et al. 2013) while deep optical imaging has revealed a weak tidal tail to the north-west and a tidal fan extending southeast from the galaxy (Tal et al. 2009). These disturbed features suggest that NGC 4261 went through merging or tidal interactions with another galaxy within the past 1-2 Gyr.

In this paper we present a detailed low-radio-frequency spectral study of the galaxy NGC 4261. Previous studies have left the question of the radiative age of the source unclear and with our study will try to resolve this problem. Our work is based on archival data from the Giant Metrewave Radio Telescope (GMRT) at 610 MHz and 240 MHz and the Very Large Array (VLA) at 1.45 GHz and 4.8 GHz. The primary goals of this work are to determine the radiative age of 3C 270 and to understand the energetics and dynamics of the interaction between the relativistic plasma of the radio lobes and the X-ray emitting gas following O’Sullivan et al. (2011). The paper is organised as follows. In Sections 2 and 3 we describe the GMRT and VLA archival data used and the data reduction. The radio images are presented in Section 4. In Section 5 we derive the physical properties of the radio source. In Section 6 we discuss our results and consider the development of the radio source in the context of its environment. The summary and conclusions are finally presented in Section 7.

We adopt a distance to NGC 4261 of 31.3 Mpc, which gives an angular scale of $1'' = 0.151$ kpc. This is consistent with the distance adopted by Worrall et al. (2010) and negligibly different from the distance adopted by O’Sullivan et al. (2011) who used an angular scale of $1'' = 0.153$ kpc for their X-ray analysis. When correcting for redshift we adopt a value of $z=0.007378$ (Cappellari et al. 2011). The radio spectral index $\alpha$ is defined according to $S_\nu \propto \nu^{-\alpha}$, where $S_\nu$ is the flux density at the frequency $\nu$.

2 GMRT OBSERVATIONS AND DATA REDUCTION

NGC 4261 was observed using the GMRT at 240 MHz and 610 MHz with total integration time of 4.5 hours in each band. At 610 MHz the data were recorded using the lower and upper side bands for an observing bandwidth of 16 MHz each. For the 240 MHz data only one correlator was used to record the data in a total observing bandwidth of 16 MHz where only half of the data were useful. Data for both frequencies were collected with 256 channels at a spectral resolution of 125 kHz per channel. The data were analysed and reduced using the NRAO Astronomical Image Processing System (AIPS) package. We summarize the details of the observations in Table 7, where we report the observing date, frequency, total observing bandwidth, total time on source, half-power beamwidth (HPBW) of the full array and rms level (1 $\sigma$) at full resolution.

The data were edited to remove bad antennas and other obvious defects. Initially the phase and flux calibrators were checked and the data with extreme phase differences were removed. This procedure was also applied to our source. The data were calibrated and the flux density scale was defined using the amplitude calibrators 3C 286 and 3C 147. The task SETJY was used to set the
Table 1. Summary of GMRT radio observations

| Project Code | Observation date | Frequency (MHz) | Bandwidth (MHz) | Integration time (min) | HPBW (full array, θ × φ) (mas) | rms (mJy beam⁻¹) |
|--------------|------------------|----------------|-----------------|------------------------|---------------------------------|-----------------|
| 15KMH01      | 2009 Feb 15      | 610            | 32              | 270                    | 7.32 ± 4.77, 76.62              | 1               |
| 15KMH01      | 2009 Feb 15      | 240            | 16              | 270                    | 15.30 ± 11.00, 67.17            | 1.6             |

Due to the large field of view of the GMRT, the field was split into multiple facets for imaging. 56 facets were created at 610 MHz (with cellsize 1.5") and 85 facets were created at 240 MHz (with cellsize 3") so that in each facet the imaging field still approximates a plane surface. When recombined for our final image these give a field of view of ∼1.2 × 1.2 at 610 MHz and ∼3 × 3 at 240 MHz. After editing again the averaged data, repeated cycles of deconvolution were performed along with careful phase-only self-calibration in order to image the data. Most of the remaining noise in our final images arises from confusion and calibration uncertainties. At the lowest frequencies the phase errors are expected to originate from rapidly varying ionospheric delays.

The final images were corrected for the primary beam pattern of the GMRT using the task PBCOR in AIPS. The rms noise level in the radio image is ∼1.6 mJy beam⁻¹. Labels indicate the individual components of the radio source. Restoring beam: 15.30 × 11.00, P.A. = 67.17°.

Figure 1. GMRT 240 MHz radio contours of 3C 270, overlaid on the R band optical image from the Digitized Sky Survey (DSS). The contour levels (black) start at 4σ and rise by factors of 2. The 1σ level in the radio image is ∼1.6 mJy beam⁻¹. Labels indicate the individual components of the radio source. Restoring beam: 15.30 × 11.00, P.A. = 67.17°.

Chandra, Ray & Bhatnagar (2004) estimate the typical uncertainty on GMRT flux measurements to be ∼5% at 610 MHz and ∼8% at 240 MHz, including contributions from the uncertainty in the measurement of calibrator flux and uncertainties introduced by the telescope hardware. These are the levels of uncertainty which we quote in Table 1. In addition, they quote an elevation dependent error on the scale of 2-4%, arising from changes in telescope response between the calibrator and source positions. These errors dominate over the systematic errors in the flux density scale.

Examination of the 610-MHz maps revealed ghost images containing up to ∼10% of the flux of the main image to the N and S of the true radio structure, presumably because of residual delay and amplitude errors, though no attempt to improve these corrections was successful. The 610-MHz image is generally similar to images with comparable angular resolution from the VLA (Section 3), but since the ghost images introduce false structure, we choose to use the 610 MHz data only for an estimate of the total flux density, and not for spectral analysis of regions within the source.

We imaged the phase and flux calibrators to check the integrity of the calibrations. While these were as expected, the flux densities derived for 8 background sources in the 3C 270 field were found to be systematically low by about 20% at 240 and 610 MHz as compared with expectations based on literature measurements. At 240 MHz all source structures appeared normal, and it was considered appropriate to increase all flux densities, including those for 3C 270, by 20%. The same procedure was applied for the total flux density of 3C 270 at 610 MHz. We note that this discrepancy cannot be resolved by using the higher 240 MHz calibrator flux for 3C 147 suggested by the Scaife & Heald (2012) scale, since this only affects one of the two calibrators, and only at one frequency.

3 VLA OBSERVATIONS AND DATA REDUCTION

From the VLA public archive we acquired and reanalysed the radio observations listed in Table 2. The data were calibrated and imaged in AIPS. In order to achieve the best possible noise level and uv coverage for the 1.55 GHz and 4.86 GHz VLA archival data, several datasets were combined for mapping. Individual observations were analysed separately until the stage where the source and calibrator uv data were separated. The SPLIT files were combined using DBCON and the analysis proceeded with phase-only self-calibration and imaging. For the 1.55 GHz data, as can be seen in Table 2, four different observations were combined together (AP0077, AV0088, AH0343 A and AH0343 B) in order to produce the final image with a total integration time of 61 minutes and an rms noise level of 0.8 mJy (Array B&C in Table 2). At 4.86 GHz only the D-array observation was used and analysed as it was sufficiently long and has a resolution comparable to the combined 1.55 GHz image. The properties of the resulting maps are given in Table 3.

The task LGEOM was used to rotate the data where needed,
Table 2. Summary of archival VLA observations

| Project | Observation date | Array | Frequency (GHz) | Bandwidth (MHz) | Integration time (min) |
|---------|------------------|-------|----------------|----------------|------------------------|
| AP0077  | 1984 Apr 23      | C     | 1.55           | $2 \times 50$  | 25                     |
| AV0088  | 1984 Jun 05      | C     | 1.49           | $2 \times 50$  | 16                     |
| AH0343 A| 1989 Mar 15      | B     | 1.57           | $2 \times 50$  | 10                     |
| AH0343 B| 1989 Jul 28      | BnC   | 1.57           | $2 \times 50$  | 10                     |
| AL0693 B| 2007 Mar 18      | D     | 4.86           | $2 \times 50$  | 81                     |

Figure 2. VLA 1.55 GHz radio contours of 3C 270 overlaid on the radio emission. The $1\,\sigma$ rms noise is $\sim 0.8$ mJy beam$^{-1}$. Contour levels start at 4$\sigma$ and rise by factors of 2. Flux Density: 18.3 Jy, Restoring beam: $15.78' \times 10.69'$, P.A. = -57.44$^\circ$.

Figure 3. VLA 4.86 GHz radio contours of 3C 270 overlaid on the radio emission. The $1\,\sigma$ rms noise is $\sim 0.4$ mJy beam$^{-1}$. Contour levels start at 4$\sigma$ and rise by factors of 2. Flux Density: 8.3 Jy, Restoring beam: $19.01' \times 11.17'$, P.A. = -55.35$^\circ$.

4 RADIO IMAGES

Figure[1] presents the GMRT 240 MHz radio image of 3C 270 at a resolution of $15.3'' \times 11.0''$ overlaid on the optical image from the Digitized Sky Survey. The contour levels start at $4\sigma$ and rise by factors of 2. The most prominent components of the source, that is, the two symmetrical bright jets and their surrounding lobes, are labelled. The VLA images at 1.55 GHz and 4.86 GHz are shown in Figures[2] and[3] respectively. The jets are more prominent on the higher-frequency maps.

The radio jets extend in opposite directions for several tens of kpc from the host galaxy of NGC 4261, having a similar morphology at all frequencies and at different restoring beams. The two bright jets are continuous and inflate two fairly round radio lobes that surround the jets. However, as expected, the prominence of the compact core increases with frequency, and it is clearly detected at 1.55 and 4.86 GHz, but not at 240 MHz.

There are two morphological differences between the two jets: first, the eastern jet bends to the north whereas the western one is straight but noticeably broadens and brightens $\sim 1-2'$ from the nucleus; second, the western lobe is slightly less extended than the eastern one. These differences may be caused by interactions with their surroundings, but we see no evidence of a denser environment on either side in the X-ray. O’Sullivan et al. (2011) note that the change in the direction of the eastern jet could be misleading, since we are viewing a projected image of a three-dimensional structure.

Table 4 summarises the properties of the source and its components including flux density, the spectral index in the 240 MHz – 1.55 GHz frequency range and the apparent linear size. The largest projected linear size of the source at all frequencies is $\sim 80$ kpc, with a total angular extent of $\sim 530''$ along the east/west axis. The jets have similar flux density and size, with the eastern jet being about 2 kpc longer, while the western jet flux density is $\sim 10\%$ greater than the eastern one. As is evident from Figures[1], [2] and[3] at lower frequencies the lobe emission extends far enough to connect the lobes north and south of the nucleus, but at 4.8 GHz no such connection is observed. This is the first clear indication of the strong spectral gradients present in the radio emission of NGC 4261.

5 RADIO SPECTRAL ANALYSIS AND PHYSICAL PARAMETERS

The archival GMRT and VLA radio data were combined with data from the literature in order to calculate the integrated radio spectrum of 3C 270. The physical parameters of 3C 270 were then calculated using the spectral index distribution of the source. The analysis described below was performed using the Synage++ package (Murgia 2000).

5.1 Spectral analysis

The integrated radio spectrum between 22 MHz and 33 GHz for 3C 270 is shown in Figure[4]. Table[5] lists the literature flux densities used in the spectrum, and the source of each measurement. Adding our VLA measurements to the literature data, we fit a Jaffe...
The maximum spatial scale resolved in our GMRT and VLA images is large compared to the source, with the possible exception of the 4.86 GHz VLA observation (∼72″, 28″, 19″ and 6″ at 240, 610, 1550 and 4860 MHz respectively). However, the VLA 1.55 and 4.86 GHz data points lie close to the fit and are both in good agreement with previous measurements at these frequencies, indicating that the VLA data capture the great majority of the flux from the source at both frequencies.

The GMRT data points are in good agreement with the model fit, suggesting that the 20% correction we applied to the GMRT flux calibration is correct. Without this correction, the GMRT 240 MHz flux density would fall ∼2.8σ below the model prediction. Including systematic uncertainties on the flux scale and the elevation-dependent error on GMRT flux calibration would bring the measurement to within 1σ of the model. However, we note that all the bright sources in the GMRT fields for which multi-wavelength data are available show systematically low flux densities; while the difference may not be strongly significant at a single frequency for 3C 270, the agreement across multiple sources and both bands suggests that the problem is real and significant.

To provide a more nuanced picture of the spectral index structure within 3C 270, we created spectral index maps of the source in two frequency ranges, 240 MHz-1.55 GHz and 1.55-4.86 GHz. Each set of images was produced in IMAGR using the same uv range, Gaussian taper and cellsize. We used a 20″ circular restoring beam (chosen based on the lowest resolution 1.55 GHz image), corrected for the primary beam, and aligned the images. Regions where the flux density in either band was <5σ significant were removed. The resulting spectral index maps are shown in Figures 5 and 6. Typical uncertainties on the spectral index in the lobes (excluding systematic uncertainties on the flux density scale) are ±0.06 for the 1.55-4.8 GHz map and ±0.05 for 240 MHz-1.55 GHz. Uncertainties in the spectral indices of the jets and core can be found in Table 4.

In Figure 5, the unresolved core of the radio source can be seen. It has a spectral index of \( \alpha_{240} \approx 0.16 \pm 0.10 \), probably as a result of self-absorption (as indicated by the lack of an obvious core in the 240 MHz image, Fig. 1, since the spectral index is rather frequency-dependent (high curvature). Moving outwards the spectral index becomes steeper and a constant value of \( \alpha \approx 0.47 \pm 0.09 \) can be seen in the jets, while the lobes that dominate the total index in the lower-frequency band appear with constant but slightly

Table 3. Summary of reduced VLA images

| Array | Frequency (GHz) | Integration time (min) | HPBW, PA (″ x ″, °) | rms (mJy beam\(^{-1}\)) |
|-------|-----------------|------------------------|---------------------|-------------------------|
| B&C   | 1.55            | 61                     | 19.0×11.2, -55.35   | 0.8                     |
| D     | 4.86            | 81                     | 15.8×10.7, -57.44   | 0.4                     |

Table 4. Radio properties of NGC 4261

| Components | \( S_{240\,\text{MHz}} \) (Jy) | \( S_{1.55\,\text{GHz}} \) (Jy) | \( S_{4.8\,\text{GHz}} \) (Jy) | \( \alpha_{240\,\text{MHz}} \) | \( \alpha_{1.55\,\text{GHz}} \) | Projected size (kpc) |
|------------|-------------------------------|-------------------------------|-------------------------------|-----------------|-----------------|----------------------|
| Total .... | 48.50±3.21                   | 18.30±0.92                   | 8.30±0.42                    | 0.41±0.08       | 1.01±0.07       | 80 × 40              |
| Core ....  | 0.48±0.04                     | 0.36±0.02                    | 0.37±0.02                    | 0.16±0.10       | 0.03±0.08       | -                    |
| West jet.  | 10.60±0.85                    | 3.80±0.19                    | 1.38±0.20                    | 0.47±0.09       | 0.90±0.15       | 37 × 7               |
| East jet.  | 8.00±0.64                     | 2.80±0.14                    | 1.13±0.06                    | 0.56±0.09       | 0.80±0.07       | 43 × 8               |

Figure 4. Radio spectrum of NGC 4261 between 22 MHz and 33 GHz. The black points are literature data, (see Table 5), and the red points are the VLA 4.86 GHz and 1.55 GHz, and the GMRT 240 MHz analysed in this paper. The best-fit curve is a Jaffe-Perola (JP) model applied to the data. The best fitting value of the spectral index at injection, \( \alpha_{\text{inj}} \), is given as well as the reduced \( \chi^2 \) value from the fit.

The slope steepens above \( \sim 5 \) GHz, with a break frequency of \( \sim 85 \) GHz, though this is likely driven to a high value owing to the high luminosity of the relatively young plasma in the jets and core. We note that a continuous-injection (CI) model gives an identical fit.
Figure 5. Map of the spectral index distribution between 240 MHz and 1.55 GHz based on images with 20$''$ HPBW. The typical uncertainty on spectral index in the lobes is ±0.05. The values within 1 beam of the sharp edges of the lobes are likely to be unreliable.

Figure 6. Map of the spectral index distribution between 1.55 GHz and 4.8 GHz based on images with 20$''$ HPBW (indicated by the circle on the lower left). The typical uncertainty on spectral index in the lobes is ±0.06. The values within 1 beam of the sharp edges of the lobes are likely to be unreliable.

steeper values ($\alpha \sim 0.60 \pm 0.09$). In Figure 5 the core is obvious with a flat spectral index $\alpha_{1550} \sim 0.03 \pm 0.08$. The steepening of the spectral index within the lobes is much clearer in this image as a spectral index of $\sim 0.9 - 1$ can be seen above and below the beginning of the jets. In the jets, the spectral index at the point where they are surrounded by the lobes is $\sim 0.5 - 0.6$ and remains constant throughout. The spectrum in the lobes gradually steepens towards the nucleus, reaching values of $\sim 1 \pm 0.06$. In both Figures 5 and 6, the features in the spectral-index maps at the edges of the source, and particularly at the ends of the lobes, are likely to be spurious and induced by residual reconstruction errors in regions of steep intensity gradient.

We performed a fit of the observed spectral index trend through the lobes using the techniques of Murgia (2003). As Figures 5 and 6 show, $\alpha_{1550}$ changes much more through the lobes than $\alpha_{2400}$, indicating that the break frequency is $\gtrsim 1.55$ GHz over most of the area. The Synage++ package only considers spectral indices between two frequencies, and we therefore use it to model the trend in $\alpha_{1550}$, while confirming that the 240 MHz data at each position do not conflict with the higher frequency data. The spectral index trend was determined by averaging the flux densities of each
Figure 7. 1.55 GHz image in grey scale. Overlaid are the 1.55 GHz contour levels starting at 3.2 mJy beam\(^{-1}\) and rising by factor of 2. The cyan circles indicate the lobe regions used for the source age estimation using the spectral index profile method.

Figure 8. Spectral-index distribution along the west lobe of the source calculated from the 1.55 and 4.86 GHz frequencies, derived using the circular regions shown in Fig. 7. The solid line represents the best JP model fit. The values of \(\alpha_{\text{inj}}\) and \(\nu_{\text{break}}\) along with the reduced \(\chi^2\) from the fit are reported here.

Figure 9. As for Figure 8 but for the east lobe.

Table 5. Integrated radio fluxes for NGC 4261 drawn from the literature

| \(\nu\) (MHz) | Flux Density (Jy) | Reference |
|-------------|------------------|-----------|
| 22.3        | 176 \pm 12       | 1         |
| 26.3        | 162 \pm 21       | 2         |
| 38          | 144 \pm 7.2      | 3         |
| 86          | 81.5 \pm 1.1     | 4         |
| 178         | 56.5 \pm 2.8     | 3         |
| 750         | 27.15 \pm 0.23   | 5         |
| 1400        | 18.62 \pm 0.93   | 3         |
| 2695        | 12.79 \pm 0.64   | 3         |
| 5000        | 8.26 \pm 0.15    | 6         |
| 10700       | 4.69 \pm 0.28    | 7         |
| 23000       | 2.6 \pm 0.1      | 8         |
| 33000       | 2.1 \pm 0.2      | 8         |

REFERENCES.-(1) Roger et al. (1969); (2) Viner & Erickson (1975); (3) Kellermann et al. (1969); (4) Artzuk et al. (1969); (5) Pauliny-Toth et al. (1966); (6) Pauliny-Toth & Kellermann (1968); (7) Kellermann & Pauliny-Toth (1973); (8) WMAP, Bennett C. L. et al. (2003)

5.2 Physical parameters of 3C 270

To calculate the key physical parameters of 3C 270, we have to make certain assumptions. Firstly, the relativistic particle and magnetic field energy densities were assumed to be uniformly distributed over the volume occupied by the radio source and in approximate energy equipartition. A low energy cut-off \(\gamma_{\text{min}}\) (where \(\gamma\) is the electron Lorentz factor) was introduced in the energy dis-
distribution of the radiating electrons rather than the fixed 10 MHz – 100 GHz frequency interval used in the classic equipartition equations (Pacholczyk 1970). We assumed that the magnetic field is unordered along the line of sight and used $\gamma_{min} \approx 100$ in the electron energy distribution, which corresponds to $\sim 50$ MeV.

We used the injection spectral index derived from the west lobe $\alpha_{inj}=0.5$, since this is in broad agreement with the value for the east lobe and the source as a whole. The flux density at 240 MHz (Table 7) was used to calculate the radio luminosity of the source, since among the frequencies used in this work it is least affected by electron spectral ageing. As the lobes are not well described by simple ellipsoids, we divided them into a number of rectangular regions chosen to approximate the breadth of the lobe at a range of distances along the jet axis. These are shown in Figure 10. Excluding the jets from the equipartition calculations for the lobes, we assume rotational symmetry about the jet axis to estimate the volume in each cylindrical region. We then group the regions, numbering these groups 1-8, to match the radial binning of the IGM pressure profile derived from X-ray observations. We also assume that the axis of the radio galaxy is in the plane of the sky. If the jet axis is oriented at $76^\circ$ to the plane of the sky (as suggested by the most recent modelling, Laing & Bridle 2014), our estimated volume will increase by $\sim 10\%$, altering our estimate of equipartition magnetic field by $\sim 10\%$.

The volumes, flux densities, spectral indices and equipartition magnetic field in regions 1-8 are listed in Table 7. We also estimated the pressure of the relativistic plasma in each region, which is defined to be

$$P_{radio} = \frac{B_{eq}^2}{2\mu_0 \rho} + \frac{(1+k)E_e}{3V}\phi,$$

where $E_e$ is the energy of the electron population, $V$ is the volume, $\mu_0$ is the permeability of free space ($4\pi$ in cgs units or $4\pi \times 10^{-7}$ in SI), $\phi$ is the filling factor of the plasma (assumed to be 1) and $k$ is the energy ratio of the non-radiating particles to the radiating relativistic electrons. We assume $k=1$, indicating equal energy in radiating and non-radiating particles. The factor $\epsilon$ describes the ordering of the magnetic field and we adopt $\epsilon = 3$, indicating a tangled magnetic field, as in O’Sullivan et al. (2011).

We find $B_{eq} \sim 5 \mu G$ for both eastern and western lobes, though the outer parts of the lobes (regions 4 and 8) have higher $B_{eq}$, close to the estimate for the source as a whole $\sim 6.4 \mu G$. For this field (see later), electrons at $\gamma_{min}=100$ radiate at $\sim 5$ MHz.

### 5.3 Radiative age

When considering the development of the radio jets and lobes, we adopt a simple conceptual model, in which at any given time plasma is rapidly transported out from the central engine to the tip of the jet. At this point the jet flow is halted by contact with the IGM, and the plasma driven out of the jet moves out radially to form the lobe. In this model, the age of the lobe plasma is linked to the distance along the jet; the back of the lobes (close to the nucleus) formed when the jet only extended a few kiloparsecs, while the tips of the lobes have only formed recently. In principle, backflows could develop, transporting younger plasma away from the jet tips into regions of the lobe formed at earlier times. However, in the absence of such a flow, or external forces causing reacceleration, plasma in the lobes is expected to age passively, with the high-frequency break in its spectral index falling to lower frequencies over time.

The radiative age of the radio source of NGC 4261 can be calculated if the break frequency of the source is known (e.g., Myers & Spangler 1984). The magnetic field is considered to be uniform and constant over the whole of the source lifetime when radiative losses dominate over expansion losses. Neglecting reacceleration processes, the radiative age (the time since the last period of injection of relativistic electrons began) can be obtained as

$$t_{rad} = 1590 \frac{B_{eq}^{0.5}}{B_{eq}^2 + B_{CMB}^2} [(1+z)t_{break}]^{-0.5} \text{Myr},$$

where $t_{break}$ is expressed in GHz, and $B_{eq}$ and $B_{CMB}$ in $\mu G$ (Parma et al. 2007). $B_{eq}$ is the equipartition magnetic field and $B_{CMB} = 3.2$ is the equivalent magnetic field strength of the cosmic microwave background (CMB) radiation at zero redshift, and equation 2 thus includes both inverse Compton and synchrotron losses.

Using equation 2 and the mean magnetic field for the source, 5 $\mu G$, we estimated a radiative age of $\sim 29$ Myr for the western lobe and $\sim 37$ Myr for the eastern one. We also derived an estimate of the advance speed of the lobe tip, $v_{adv}/c$, where $c$ is the speed of light. This velocity was calculated as $v_{adv} = LD/t_{rad}$, assuming a constant simple velocity and using the linear distance (LD) from the back of the lobe to the tip of the jet as measured from the radio images in Section 4. We found that for both lobes $v_{adv} \sim 0.004c$ ($\sim 1300$ km s$^{-1}$ for the western lobe and $\sim 1200$ km s$^{-1}$ for the eastern one).

By comparison, the sound speed in the IGM in the environment around NGC 4261, estimated from the measured X-ray temperature, increases from about 380 km s$^{-1}$ near the core to 590 km s$^{-1}$ beyond $\sim 100\'$. The advance speed of the lobe tip therefore appears to be supersonic relative to the IGM. Conversely, the Alfvén speed in the lobe is about $10^5$ km s$^{-1}$ (using the lobe plasma properties deduced in Section 5.2). That is, speed of expansion of the lobe is strongly sub-Alfvénic, and so will not excite magnetic shocks in the lobes. The internal characteristic speed of the waves in the magnetized relativistic plasma were calculated from

$$\epsilon = 3 \text{ and } \gamma_{min} = 100 \text{ radiate at } \sim 5 \text{ MHz.}$$

| Region | $\alpha_{inj}$ | $t_{break}$ (GHz) | $t_{rad}$ (10$^6$ yrs) | $v_{adv}$ |
|--------|----------------|-------------------|-----------------------|----------|
| West lobe | 0.56$^{+0.04}_{-0.03}$ | 12.4$^{+4.3}_{-2.7}$ | 29$^{+3}_{-4}$ | $\sim 0.004c$ |
| East lobe | 0.50$^{*}$ | 7.5$^{+3.0}_{-0.4}$ | 37$^{+1}_{-2}$ | $\sim 0.004c$ |

Figure 10. Regions used for the estimation of the volume and the other physical parameters described in Table 7. The 3.2 $\mu Jy$ (4$\sigma$) contour is shown to indicate the limit of the detected lobe emission.
Table 7. Physical parameters of 3C 270 and its components

| Region     | \( r_{\text{min}} \) (arcsec) | \( r_{\text{max}} \) (arcsec) | \( V_{\text{tot}} \) (kpc) | \( S_{2400\text{MHz}} \) (mJy) | \( S_{1550\text{MHz}} \) (mJy) | \( \alpha_{\text{obs}} \) | \( L_{1550} \) (10^{22} W/Hz) | \( B_{\text{eq}} \) (\( \mu \)G) | \( P_{\text{radio}} \) (10^{-12} dy cm^{-2}) |
|------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| West Lobe  |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 1          | 10              | 33              | 1724            | 998 ± 80        | 316 ± 16        | 0.62            | 3.6             | 5.0             | 1.42            |
| 2          | 33              | 63              | 3861            | 2067 ± 165      | 650 ± 33        | 0.62            | 7.3             | 4.9             | 1.36            |
| 3          | 63              | 168             | 12081           | 8741 ± 700      | 3138 ± 157      | 0.55            | 35              | 5.5             | 1.73            |
| 4          | 168             | 242             | 2551            | 2262 ± 181      | 897 ± 45        | 0.50            | 10              | 6.0             | 2.06            |
| East Lobe  |                 |                 |                 |                 |                 |                 |                 |                 |                 |
| 5          | 10              | 33              | 1056            | 408 ± 33        | 146 ± 7         | 0.55            | 1.6             | 4.6             | 1.21            |
| 6          | 33              | 63              | 1646            | 976 ± 78        | 287 ± 14        | 0.66            | 3.2             | 4.9             | 1.39            |
| 7          | 63              | 168             | 9753            | 5868 ± 469      | 2310 ± 116      | 0.50            | 26              | 5.3             | 1.64            |
| 8          | 168             | 282             | 4668            | 5755 ± 460      | 2202 ± 110      | 0.52            | 25              | 6.5             | 2.43            |

\[ v_A = \frac{c}{\sqrt{1 + \frac{u_{\text{rel}} + P_{\text{radio}}}{2P_{\text{mag}}}}} \]  

where \( v_A \) is the Alfvén speed expressed in m s\(^{-1}\), \( u_{\text{rel}} \) is the energy density of the relativistic particle population, and \( P_{\text{mag}} \) is the magnetic field pressure.

6 DISCUSSION

6.1 The age of the source

Before considering the implications of our radiative age measurements, we first discuss potential sources of error in our approach. We have performed a relatively simple modelling of the 1.55-4.86 GHz spectral index trend in the lobes, which our model relies on a number of assumptions. These include constant source expansion velocity, constant magnetic field, our choice of spectral model, and that reacceleration, adiabatic expansion and mixing is not important processes in the lobes. As mentioned in Section 5.1, the fact that our model provides a reasonable description of the spectral index trend suggests that the assumption of a constant expansion velocity is at least reasonable; we see no evidence that velocity changes are required, though our other factors could displace deviations from the trend. As a further test, we refitted the spectral index profiles, adding one additional region closer to the AGN. In both lobes, the fits were poorer, primarily because of the differences in the extent of the emission seen in the lobes close to the nucleus (back of the lobes) at 1.55 and 4.8 GHz, which lead to divergence from the smooth trend in spectral index. For example, in the west lobe, the added region is close to the edge of the lobe at 4.8 GHz, leading to a steeper than expected spectral index and a reduced \( \chi^2 \). Both fits find lower break frequencies \( \sim 5 \) GHz, suggesting radiative ages \( \sim 45 \) Myr, older than our best estimate, but not by a large factor.

Our use of the JP model may be over-simple, but we are limited in this by the available data. Harwood et al. (2013) compare the utility of several spectral models to describe spectral ageing in FR-II galaxies and conclude that the Tribble (1993) model provides the best combination of fit quality and physical realism; Harwood et al. consider the JP model at least as physically accurate, but it provides a poorer fit. However, they find that to differentiate between models requires data at 7-9 frequencies, whereas we have only 3 available. Further observations are therefore needed to determine whether a different model might provide a better description (and age estimate) for 3C 270.

Losses caused by adiabatic expansion would affect our age estimate, lowering the break frequency and therefore the estimated age. However, adiabatic losses decrease the luminosity of the plasma, and are more effective in doing so than they are in reducing \( v_{\text{break}} \). We might expect losses in the jets as they flare from the narrow collimated structures seen in the X-ray to the broad jets we observe in the radio, but the fact that the lobes have high surface brightnesses and smooth surface brightness distributions suggests that adiabatic losses within the lobes are probably not important. Variation in the magnetic field within the lobes could affect our results, but on large scales we only measure a relatively small \( (\sim 20\%) \) change in field strength across the lobes (see Table 7, perhaps as little as 8% in the radius range used to estimate age. This is insufficient to balance the observed spectral index trend, and we therefore consider our assumption of a constant field to be a reasonable approximation. Small-scale field variations cannot be ruled out, but would again require improved spectral modelling and additional observations.

Moving on to the results, our spectral-index profile modelling (Figures 5 and 6) implies ages of \( t_{\text{rad}} \) \( \sim 29 \) and 37 Myr for the west and east lobes respectively (Table 6). These ages are less than the \(<75\) Myr upper limit estimated by O’Sullivan et al. (2011) from the IGM sound speed. While the upper limit and our values are consistent, the factor two difference between the values seems to be significant; Eilek (1996) first noted that the synchrotron ages for FRI and FRII radio sources derived from the spectra differed from the dynamical ages as much as a factor of 10. By this standard the factor of 2 discrepancy we observe is relatively mild. Several studies suggest plausible explanations for the age difference between spectral and dynamical ages (Blundell & Rawlings 2000), including in situ acceleration of particles (e.g., Eilek 1996; Carilli et al. 1997) and magnetic fields that vary with position in the lobes (e.g., Katz-Stone et al. 1993; Eilek & Arendt 1996). Studies have shown much better agreement between dynamical and spectral ages in young sources (<10 Myr, Matthews & Scheuer 1990; Kaiser et al. 1997), but the cause of the discrepancy in older sources is still unknown. We will discuss three possible explanations for the age discrepancy in 3C 270: i) a period of highly supersonic expansion early in the AGN outburst; ii) multiple outbursts or large changes in jet power; iii) a backflow capable of mixing younger electrons from the jets into the old plasma at the back of the lobes.

In scenario (i), the expansion of the lobes was much faster in the past, so that the assumption of a constant near-sonic expansion velocity by O’Sullivan et al. (2011) leads to an overestimate of the age of the source. For the larger eastern lobe, the radiative age
(37 Myr) implies that the lobes should be driving into the IGM at Mach ~2, if they have expanded at constant velocity. Shocks in the IGM, driven by this expansion, would be detectable in the available X-ray observations as increases in temperature and surface brightness, and are ruled out by the measurements described in O’Sullivan et al. (2011). However, there is also the possibility of that a period of supersonic expansion occurred early in the life of the source, followed by a period of slower expansion which we are now observing. In this case, the shocks would have detached from the lobe tips as the expansion speed dropped, and moved outwards, potentially passing out of the field of view of the XMM-Newton observation. Assuming that the shock front is just outside the XMM field of view (~14′ or ~130 kpc) we can calculate the duration of the supersonic phase. The minimum Mach number of such a shock would be $M_{\text{min}} \sim 6$ (~3500 km s$^{-1}$). The corresponding maximum period of supersonic expansion would be ~7.5 Myr, during which time the lobes would expand to ~28.5 kpc along the jet axis. After this, expansion would continue at the sound speed for the remaining 3/4 of the lifetime of the radio source.

A Mach~6 shock in the IGM would cause an increase in X-ray surface brightness of a factor ~13.5 and a temperature increase of a factor ~12. Even if the efficiency of energy deposition is low, such a shock would have strongly heated the IGM, and the observed temperature would be the result of this heating. For a 10% heating efficiency, we would expect the shock to have deposited $\sim 10^{40}$ erg in the central 10 kpc alone, and the current rate of radiative energy loss, $\sim 10^{41}$ erg s$^{-1}$ would only have removed ~1% of this energy. This implies a pre-shock core temperature as low as 0.1 keV, lower than is observed in any group or cluster, and more comparable with the temperature of the interstellar gas in our own Galaxy than that expected in a giant elliptical. Since NGC 4261 appears to be fairly typical of the population of group and cluster-central FR-I radio galaxies, we might also expect to see a population of such sources driving shocks of similar strength, with evidence of strong shock heating. No such population has been identified. The scenario of a single, highly supersonic outburst therefore seems unlikely.

In scenario (ii) the AGN would have undergone more than one outburst, or the jet power may have varied significantly over time. In this case our estimated age could correspond to the newest outburst or period of high jet power. A restarted jet, or period of more powerful outflow, could drive shocks into the lobes, causing in situ reacceleration in the old plasma while producing new expansion at the lobe tips. Worrall et al. (2010) note structure that could be caused by variations on $\sim 10^4$ yr timescales in the X-ray jet, while the changes in radio brightness along the western jet suggest variation on longer timescales. This scenario is plausible, and difficult to rule out with current data.

In scenario (iii) a backflow would transport young, energetic electrons back towards the nucleus, reducing the mean age of the plasma. Numerical simulations (e.g., Perucho & Martí 2007) support the possibility of mildly relativistic backflows in a sheath surrounding light FRI jets. Modelling of the base of the jets in 3C 270 does not reveal any evidence of such a backflow (Laing & Bridle 2014), but it cannot be ruled out on larger scales. However, if backflows are limited to a sheath around the jets (Laing & Bridle 2012), the question of how electrons are mixed outwards into the larger lobe remains. A bulk backflow, with transport of and mixing of plasma throughout the lobe would be required, but seems less plausible given the lobe morphology.

Considering the merits of these three possibilities, we favour scenario (ii), and suggest a model for the expansion history of the source in which, 75 Myr ago, an outburst swept its way through the X-ray gas, beginning the excavation of the cavities. These cavities grew in stages as the jet power varied over time, with the lobe plasma being refreshed by each new outburst or period of high jet power, the most recent of which is only ~30 Myr old. The overall lobe/cavity inflation time would thus be similar to the X-ray estimate, but the plasma we see in the lobes is a mixture of old and new particles injected by a period of stronger jet activity over the last ~30-40 Myr.

6.2 Pressure balance and particle content

The non-thermal energy density in the lobes of an extended radio source cannot be determined by the radio data alone. Only a minimum value can be estimated when we assume the contribution from the magnetic field and the relativistic particles equal (Burbridge 1958). The additional information needed to constrain the internal energy density can be obtained either from measurement of the inverse-Compton emission caused by the up-scattering of photons off the relativistic electrons in the lobes, or by assuming pressure equilibrium between the lobes and their environment and measuring the IGM pressure using X-ray data (Longair et al. 1975).

We first test our ability to detect inverse-Compton emission from the lobes. Assuming equipartition, O’Sullivan et al. (2011) estimated an expected X-ray flux density from up-scattered cosmic microwave background (CMB) photons to be ~2 nJy from each lobe at 1 keV. Using our improved constraints on the properties of the lobe plasma, we repeat this calculation, and find that we expect a flux of $\sim 6.5 \times 10^{-14}$ erg s$^{-1}$ in the 0.5-7 keV band (~4.1 nJy at 1 keV) from each lobe. We then reprocessed the longest XMM-Newton dataset available (ObsID 0502120101, ~70 ks after cleaning) using the latest calibration and most recent version of the XMM Science Analysis System (sas 13.5). Following the techniques described in O’Sullivan et al., we find no detection of inverse-Compton flux from the lobes, but are able to place 3σ upper limits on the 0.5-7 keV flux of $< 6 \times 10^{-14}$ erg cm$^{-2}$ s$^{-1}$ (< 3.8 nJy) for the west lobe, and $< 6.2 \times 10^{-14}$ erg cm$^{-2}$ s$^{-1}$ (< 4.0 nJy) for the east lobe. These limits are marginally below the predicted flux, and so may suggest that the lobe plasma is out of equipartition, with more energy in the magnetic field than in the particle population. However, the uncertainties in the radio fluxes, XMM calibration (see, e.g. Nevalainen et al. 2010) and the choice of X-ray spectral model only weakly constrain departures from equipartition in the sense of domination by the electron (and positron) energy density. Deeper X-ray data are needed to provide a lower flux limit and determine whether the lobes are truly in equipartition.

We also estimated the likely optical flux in the inner part of the lobes from up-scattering of infra-red photons emitted by the stellar population. Unfortunately, the expected signal is low, a factor $\sim 10^{-3}$ below the optical luminosity of the stellar population in the same region. We are therefore unable to constrain the properties of the lobe emission from its inverse-Compton emission, at least with the currently available data.

As inverse-Compton emission does not provide a definitive constraint, we compare the apparent lobe pressure with that of the surrounding IGM. Figure 11 shows the pressure profiles of the thermal gas ($P_{\text{gas}}$) along with the profile of the radio pressure derived in this study, as a function of the distance from the source’s centre. The X-ray pressure profile is drawn from the XMM-Newton analysis of O’Sullivan et al. (2011). As can be seen from Fig. 11 the X-ray pressure profile declines with radius as expected, while the pressure profile derived from the radio lobes rises with radius.
The radio lobes appear to be underpressured with respect to the surrounding environment in all regions and in both lobes by a factor ranging from \(\sim 2\) to \(\sim 30\). We note that the [O’Sullivan et al. (2011)](O'Sullivan et al. 2011) IGM pressure profile is in excellent agreement with the earlier measurements of [Croston et al. (2008)](Croston et al. 2008), but that Croston et al. found a mean internal pressure for the radio lobes of \(\sim 9 \times 10^{-13}\) erg cm\(^{-3}\), slightly lower than the pressures we measure in the lobes.

A similar pressure imbalance has been found in previous lobe studies of other FR I radio sources, where \(P_{\text{gas}}/P_{\text{radio}}\) is usually \(> 1\), reaching values up to 100, assuming the standard equipartition arguments (e.g. [Feretti et al. 1992] Dunn et al. 2005) Croston et al. 2008) Birzan et al. 2008) Dunn et al. 2010). This can only suggest two possible situations for the radio lobes in the case of 3C 270: 1) Deviation from equipartition within the radio lobes with a higher magnetic field energy density than calculated, or 2) the equipartition argument is still valid but either the radio lobes contain a significant amount of non-radiating particles that contribute to the internal pressure or the filling factor \(\phi\) of the plasma is less than unity. Since we believe that jets entrain material in FR I galaxies and in this specific galaxy we have reason to think the filling factor might be \(\leq 1\) at the back of the lobes (volume overestimation including part of the brighter X-ray emitting gas near the cool core), we examine the implications of the lack of pressure balance in the case where equipartition stands.

Assuming that the radio lobes of 3C 270 are in approximate pressure equilibrium with the IGM, we have the ability to constrain the particle content of the lobes from the comparison of the apparent pressures of the relativistic plasma of the radio lobes and that of the thermal plasma of the IGM (e.g., Hardcastle & Worrall 2000) Birzan et al. 2008).

In Table 8, the results shown for \((1 + k)/\phi\) estimation were calculated by forcing \(P_{\text{radio}}\) to equal \(P_{X\text{ray}}\) (note that in Table 6 we adopted a fixed \((1 + k)/\phi = 2\)). The regions of the radio pressure in this study were chosen so as to match the X-ray annuli used by [O’Sullivan et al. (2011)](O’Sullivan et al. 2011). Both lobes show the same trend with the \((1 + k)/\phi\) factor rising as we move from the end of the jets (regions 4 and 8) to the back of the lobes near the core (regions 1 and 5). The size of the bins were not exactly equal so the increase of \((1 + k)/\phi\) is not linear.

Assuming that the filling factor \(\phi = 1\), the additional pressure required by the rise of \((1 + k)/\phi\) in regions 2-4 and 6-8 can be provided by non-radiative particles in the relativistic plasma of the lobes. This non-radiating component could be introduced via the entrainment and heating of thermal plasma by the radio jets. A probable source of entrained material is stellar mass loss from stars within the jets (Phinney 1983) Komissarov 1994) Hardcastle et al. 2003) 2007). In [O’Sullivan et al. (2011)](O’Sullivan et al. 2011) the rate of stellar mass-loss from AGB stars into each jet was estimated to be \(1.67 \times 10^{-3}\) M\(_{\odot}\) yr\(^{-1}\). By assuming a 37 Myr timescale for the AGN outburst, we expect a minimum of \(\sim 60000\) M\(_{\odot}\) of stellar material to be entrained by each jet.

Thermal plasma entrained from stars within the radio jets represents a plausible minimum mass of entrained material. Taking the limiting assumption that in regions 4 and 8 the only entrained material is that from stars in the jets (i.e., that no additional entrainment occurs across the lobe/IGM boundary), we can estimate an upper limit on the temperature to which this thermal component must be heated in order to bring the lobes into thermal balance with their surroundings. We find the temperature of the entrained material to be \(k_B T \lesssim 11\) MeV which corresponds to a plasma with electrons having a Lorentz factor \(\gamma \lesssim 20\), well into the relativistic regime. Electrons of \(\gamma \sim 20\) are expected to radiate in the equipartition magnetic field at \(\sim 1\) kHz, making them invisible in the observable radio band. Comparable values have been found by applying similar arguments to Cen A (Wykes et al. 2013) and 3C 31 (Croston & Hardcastle 2014). The very low density of this entrained thermal plasma component (\(\sim 1.4 \times 10^{-7}\) cm\(^{-3}\)) means that no significant thermal or non-thermal X-ray emission is expected from it. By summing up \((P_{X\text{ray}} - P_{radio}) V\) from each region, where \(V\) is the volume of each region, we estimate that the total energy (Table 8) required to heat all the entrained material in the lobe to 11 MeV is \(\sim 9 \times 10^{57}\) erg.

Alternatively, pressure balance could be produced if the filling factor \(\phi < 1\). This could occur in several ways, for example if we have overestimated the lobe volume or if significant variations in the density of relativistic particles and magnetic field exist within the lobes.

The most likely location in which \(\phi\) may be \(< 1\) is in regions 1 and 5, which have values of \((1 + k)/\phi\) much greater than those of the neighbouring regions. Since regions 1 and 5 of the lobes overlap with the brighter X-ray emission north and south of the cool core, it is possible either that our assumption that the morphology of the lobe can be described as an annulus in this region is oversimplified, or that the lobe and IGM plasmas are mixed, with filaments or clouds of IGM gas penetrating the volume apparently occupied by the lobe. If we estimate the value of \(k\) based on the increase in \(k\) from regions 1-3 and 5-7, we find that we would expect \(k \sim 24\) for region 1 and \(k \sim 23\) for region 5. This suggests that \(\phi\) could be as low as \(\sim 0.59\) for region 1 and \(\sim 0.48\) for region 5.

If thermal plasma is present in the lobes, we would expect it to cause Faraday rotation. We can therefore compare our expected density of entrained material with limits derived from the rotation measures for 3C 270 found by [Guidetti et al. (2011)](Guidetti et al. 2011) and [Laing & Bridle (2014)](Laing & Bridle 2014). While these measurements include the effects of external Faraday rotation, they do provide an upper bound on the internal rotation measure. Following [Feretti et al. (1999)](Feretti et al. 1999) we calculate the expected rotation measure from:
where RM is the rotation measure in rad m$^{-2}$, $n_e$ is the electron number density in cm$^{-3}$, $B_z$ is the magnetic field along the line-of-sight in μG and L is the integration path (the depth of the lobe along the line-of-sight) in kpc. Based on the Guidetti et al. and Laing & Bridle results, an RM of order 10 rad m$^{-2}$ seems representative for the system. We find that an electron gas density of $\sim 8.2 \times 10^{-5}$ cm$^{-3}$ would be required to produce RM=10 rad m$^{-2}$ purely from internal depolarization. The expected electron density of thermal plasma entrained in the lobes ($\sim 1.4 \times 10^{-7}$ cm$^{-3}$) is low compared to this limit, and would be expected to produce RM$\sim 0.02$ rad m$^{-2}$, well below the sensitivity of the Guidetti et al. maps. We therefore agree with the conclusion drawn by Guidetti et al., that the RM structures they observe are probably caused by foreground depolarization.

We can also test whether regions 1 and 5, which we earlier suggested have filling factors less than unity, could contain a mix of thermal and relativistic plasmas, or whether it is more like that our adopted geometry leads us to overestimate their volume. Using equation (4) and the IGM electron density derived from the X-rays in O’Sullivan et al. (2011) we find that we expect an internal RM of $\sim 500$ rad m$^{-2}$ for both regions. While Guidetti et al. (2011) do find evidence of enhanced depolarization at the inner edges of the lobes, our predicted value is a factor $\sim 20$ higher than they observe. This indicates that the relativistic and thermal plasmas along these lines of sight are probably not well mixed. This could suggest that the geometry we have assumed for the lobes close to the core is too simple, for example if filaments or sheets of thermal plasma penetrate the lobe while remaining magnetically separate. Alternatively, the internal properties of the lobe plasma may differ in these regions from those seen through the rest of the lobes.

In O’Sullivan et al. (2011) the total enthalpy, 4PV - the energy required to expand the lobe to its current size against the pressure of the IGM, plus the energy stored in the magnetic field and particles in the lobe - was estimated to be $\sim 2.4 \times 10^{58}$ erg. Our energy estimate of $\sim 9 \times 10^{57}$ erg required to heat any entrained material is about 40% of the enthalpy estimated by O’Sullivan et al., mainly owing to our more accurate treatment of lobe volume. The estimate changes little if the lower filling factors in regions 1 and 5 are adopted.

In summary, we have examined the constraints which can be placed on the particle populations in the radio lobes from the available radio and X-ray measurements. We find that only a relatively small mass of entrained gas is needed to bring the lobes into pressure equilibrium with their surroundings, that this is probably consistent with entrainment of stellar material lost from stars within the jets, and that such material would have a low density and therefore would not have detectable effects on the polarization.

### 7 CONCLUSIONS

In this paper, we have presented a detailed spectral analysis of the FR I radio source 3C 270, emanating from the nearby group-central elliptical galaxy NGC 4261. We have analysed 240 MHz and 610 MHz data from the GMRT, and data from the VLA at 1.55 GHz and 4.86 GHz.

Combining the analysed GMRT and VLA data with data flux density measurements from the literature between 22 MHz and 33 GHz, we used a Jaffe & Perola (JP) model to determine the asymptotic low-frequency spectral index of 3C 270 to be $\alpha_{\nu_{\text{inj}}} = 0.5^{+0.02}_{-0.02}$. From the GMRT 240 MHz and VLA 1.55 GHz and 4.8 GHz, we produced spectral index maps of the source which suggest a spectral index of $\alpha \sim 0.16$ for the unresolved and probably self-absorbed core, a constant spectral index along the jets of $\alpha \sim 0.5$ and a gradual steepening from the tip of the jets through to the back of the lobes of $\alpha \sim 0.8 \pm 1$.

Assuming equipartition of energy between the magnetic field and the relativistic particles, and adopting a minimum Lorentz factor of $\gamma_{\text{min}}=100$ for the radiating electrons, we estimate the radiative age of 3C 270. We modelled the observed 1.55-4.86 GHz spectral index trend in the lobes, fitting a Jaffe & Perola (JP) model. We find a radiative age of $t_{\text{rad}} \sim 29$ and 37 Myr for the west and east lobes respectively. This is about half the dynamical age of <75 Myr found previously using X-ray data (O’Sullivan et al. 2011). We considered three possible scenarios for this discrepancy. The least likely is that the source underwent an early period of supersonic expansion. While the shocks from such an expansion might now be outside the field of view of the available X-ray observations, they would have very significantly heated the IGM, implying unphysically low pre-shock temperatures.

A second alternative is that a backflow within the lobes may be transporting young, energetic electrons from the jet into regions of older plasma, leading us to underestimate the age. This cannot be ruled out, but previous high resolution observations of the base of the jets do at least argue that no backflow is observed on small scales. Finally, the third possibility, which we favour, is the
observed source is the product of multiple AGN outburst or large change in jet power, with the radiative age corresponding to the latest outburst or period of high jet power. Worrall et al. (2010) noted structures in the X-ray jet that could be indicate variations in power on 10^4 yr timescales, and larger scale variations in jet brightness are observed in the radio. A renewed outburst would not only inject a fresh population of young electrons into the lobes, but would likely drive shocks into the only population, causing reacceleration. The end result would be a source whose lobe expansion time might be similar to the X-ray age estimate while the radiative age represents the onset of more recent activity.

Assuming that the pressures in the radio lobes equal that of the IGM we calculate that the ratio of energies of non-radiating to radiating particles, k, ranges from $\sim 4 - 24$ from the tip of the jets to the lobes close to the core (Table 8, Fig. 10). This suggests that gas entrainment was more effective at earlier times, when the jets were shorter. Assuming, as a limiting case, that currently only material lost from stars in the jets is entrained, we estimate that the temperature of the entrained material would need to be 11 MeV if material lost from stars in the jets is entrained, we estimate that the temperature of the entrained material would need to be 11 MeV if it is to bring the lobes into pressure balance with the IGM. This corresponds to a total energy of $\sim 10^{58}$ erg required to heat the entrained material in the lobe, $\sim 40\%$ of the total enthalpy of the lobes estimated in O'Sullivan et al. (2011).

Based on our estimates of the density of the entrained material, we predict the likely internal rotation measure arising from this component, and compare it to RM measurements from the literature. The density of $\sim 1.4 \times 10^{-7}$ cm$^{-3}$ indicates that the contribution of the entrained material to the Faraday depolarization is undetectable. In regions 1 and 5 where the thermal X-ray emitting plasma co-exists with the relativistic plasma, we would expect a RM of $\sim 500$ rad m$^{-2}$ for both regions if mixing had taken place. This is ruled out by the observations, implying that little mixing between the thermal and relativistic plasmas has occurred.

ACKNOWLEDGMENTS

K. Kolokythas is supported by the University of Birmingham. E. O’Sullivan acknowledges support for this work from the National Aeronautics and Space Administration through Chandra Award Number AR3-14014X issued by the Chandra X-ray Observatory Center, which is operated by the Smithsonian Astrophysical Observatory for and on behalf of NASA under contract NAS8-03060, and through the Astrophysical Data Analysis program, awarded NNX13AE71G. S. Giacintucci acknowledges the support of NASA through Einstein Postdoctoral Fellowship PF0-110071 awarded by the Chandra X-ray Center (CXC), which is operated by the Smithsonian Astrophysical Observatory (SAO). GMRT is run by the National Centre for Radio Astrophysics of the Tata Institute of Fundamental Research. Some of this research was supported by the EUFP7 Marie Curie award of the IRSES grant CAFEGROUPS (247653). We thank T. Ponman and Andreas Zezas for useful discussions of NGC 4261 and formation history. We thank the anonymous referee for his help in improving the paper.

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