Glacial lake outburst floods (GLOFs) are a hazard commonly reported in the glaciated terrain of the Himalaya. Glacier lakes can form if the glaciers retreat and the bottom topography overdeepens. We have adopted a technique to estimate the depth and volume of lakes using parameters such as glacier surface velocity, slope and laminar flow of ice. The technique has been automated using Python programming language. The method was applied in the Sikkim Himalaya to map potential lake sites and also to predict further expansion of existing glacier lakes. Studies were carried out for ten glaciers in the Tista river basin. The analysis suggests nine potential lake sites, including further expansion of four existing glacier lakes. To validate the results, the model lake boundary in 2001 was compared with the satellite-observed value of 2015 and field measurements made at the South Lhonak lake. The volume of the South Lhonak lake (in 2015) was estimated as 60 $\pm$ 10.8 million m$^3$; with prolonged retreat of the glacier, the lake is likely to expand to a maximum volume of 90 $\pm$ 16.2 million m$^3$. The above technique can provide new information to planners, leading to a more realistic approach in understanding the disaster potential of glacier lakes.

Keywords: Glacier lakes, depth and volume estimation, remote sensing, disaster potential, over deepening.

In recent decades, the Himalayan glaciers are thinning and retreating due to changes in climate$^{1-3}$. Depending upon geomorphological conditions, retreating glaciers can lead to the formation of moraine-dammed lakes$^{4,5}$. If overdeepening is sufficiently large, it results in further expansion of the lake and this could be a potential source of flash floods. Many such flash floods have been reported in the Himalaya. One of the earliest glacial lake outburst floods (GLOFs) was reported in the Shyok glacier, Jammu and Kashmir, India in 1926, which destroyed Abudan village and the surrounding land$^6$. Other events were reported in the Kinnaur valley, Himachal Pradesh during 1981 and 1988 (ref. 7). In addition, the flash flood in kedarnath in 2013 with heavy rainfall in the surrounding areas was possibly due to an outburst of the Chorabari lake$^8$. To assess future floods, estimation of potential volume of new glacier lakes and further expansion of existing lakes is needed$^9,10$.

Remote sensing techniques have been extensively used to identify and monitor moraine-dammed lakes in the Himalaya$^{11–16}$. These studies were carried out in the Satluj, Chenab, Ganga, Tista, Chandra, Zanskar and Central Himalayan river basins, where a large number of glacier lakes were identified. Several of these lakes were reported as dangerous with the potential to cause flash floods, depending on their size and temporal behaviour$^{17,18}$. It is difficult to estimate the potential hazard from these observations due to the lack of information on depth, as remote sensing techniques cannot easily estimate depth of the lake. Therefore, approaches based on area–volume scaling were used to estimate the lake volume$^{19–23}$. However, this technique showed a large variation in volume estimates, as the scaling relationship was developed using limited data. These scaling techniques are not useful to forecast future expansion and identify potential glacier lake sites. Hence a method based on velocity, slope and laminar flow equations was adopted to estimate the location and volume of potential lakes$^{4,24}$. This method was standardized for Chhota Shigri glacier in the Himalaya and Glacier de Corbassière in the Swiss Alps$^{4,24}$. This method has been compared with other techniques to estimate ice thickness$^{25}$. In the present study, the method was applied to glaciers in the Sikkim Himalaya and lake volume was validated. This has provided important information on potential lake sites and further expansion of existing glacier lakes in the Tista river basin. The data would be valuable for modelling GLOF impacts and planning mitigation measures in Sikkim.

Study area and data

Studies were carried out in the Sikkim Himalaya. Initially, 10 glaciers covering an area of 136 sq. km were selected, wherein 4 glaciers have moraine-dammed lakes (Figure 1). Landsat ETM+ imagery of 2001/2002 and Landsat 8 (OLI/TIRS) imagery of 2015 were downloaded from the United States Geological Survey (USGS) website (https://earthexplorer.usgs.gov/) to estimate surface velocity of the
glaciers. The glacier boundaries were obtained from the Randolph Glacier Inventory (RGI) and Advanced Spaceborne Thermal Emission and Reflection Radiometer Digital Elevation Model (ASTER DEM) (http://reverb.echo.nasa.gov/reverb). The horizontal posting of ASTER DEM is 30m and vertical posting 17 m.

In situ data

The bathymetric data of South Lhonak lake were collected from an executive summary report "South Lhonak glacial lake outburst flood, North Sikkim". Field studies were carried out at the South Lhonak lake from 28 to 30 August 2014. The field survey included bathymetry survey to compute volume of water and resistivity survey to infer subsurface lithology and composition of terminal moraine. Electrical resistivity was used to estimate layered structure of sediments and distribution of ice below the moraines. Depth measurements and GPS locations were taken at approximately 200 points. The points were selected randomly and the Hondex PS-7 Depth Sounder was used for measurements. The instrument has a maximum measuring capacity of 80 m. In addition, a follow-up survey at the South Lhonak lake was done on 28 August 2016 by Sharma et al. using Hondex HE-770, which can estimate depth from 3 to 500 m. The accuracy of GPS used in the survey is 1–3 m and mean error for the echo sounder data is 2–3 m.

Methodology

To estimate the potential sites and volume of glacial lakes, the following steps were used: (i) Initially, glaciers were identified from satellite imagery of 2001 and 2002. (ii) The surface velocity of the glaciers was estimated using COSI-Corr method and depth was modelled using laminar flow of ice. (iii) A DEM and depth were used to
To estimate the spatial distribution of ice thickness, the ‘Topo to Raster’ tool in ArcGIS was used; this utilizes the discretized thin plate spline interpolation technique for interpolation\textsuperscript{23}, keeping depth of the glacier along the boundary as zero. Then, the bottom topography was estimated by subtracting glacier depth from surface elevation. The troughs in the bedrock were identified using the ArcGIS hydrology fill tool\textsuperscript{14}. The difference between the filled bed and unfilled bed topography provides an estimate of overdeepening below the existing glacier. However, when the actual lake is formed, it will also depend upon the surrounding topography of the glacier. Therefore, the topography up to the lateral moraines was considered and lateral moraines were delineated by visual interpretation. The depth of existing lakes was estimated using the shape and maximum depth, with the assumption that depth decreases as a function of distance up to shoreline\textsuperscript{35}. In case of existing lakes, the maximum bed overdeepening over the glaciated portion, as derived from the model, was extended up to the shoreline where depth was considered zero.

The uncertainties in the modelled ice thickness estimates (based on eq. (3)) are calculated using the expression\textsuperscript{4}

$$\frac{dH}{H} = \sqrt{\left(\frac{1}{4U_b} \frac{dU_b}{U_b}\right)^2 + \left(\frac{3}{4f} \frac{df}{f}\right)^2 + \left(\frac{3}{4\rho} \frac{d\rho}{\rho}\right)^2 + \left(\frac{3}{4\sin\alpha} \frac{d\sin\alpha}{\sin\alpha}\right)^2}.$$  

\textbf{Sources of uncertainty while estimating surface velocities of glaciers from satellite images}

The mean velocity on stable ground was estimated by COSI-Corr method as 3 m/year. This can be considered as an error since surface velocity of stable ground is expected to be zero\textsuperscript{36}. Other parameters such as co-registration of Landsat ETM+ and COSI-Corr accuracy can also introduce errors in velocity; the values are 5 m (ref. 37) and 1.5 m (~1/20th of a pixel) respectively\textsuperscript{24,27}. The combined error in velocity was estimated as 6 m/year.

The error in glacier areal extent was considered as 5% in the RGI data\textsuperscript{18}. The uncertainty in the shape factor value arises due to the influence of side drag along the glacier flow lines, and it varies with width of the glacier. Considering the range of values between 0.7 (ablation) and 0.9 (accumulation)\textsuperscript{28,39}, the error in shape factor was considered as ± 12.5% in the present analysis\textsuperscript{2}. The uncertainty in ice density $\rho$ was taken as 10% considering the typical variation in ice density from 830 to 923 (kg m$^{-3}$)\textsuperscript{13}. The uncertainty in $\sin\alpha$ arises due to vertical inaccuracies in DEM. Due to similarity in topography and lack of ground measurement data in the present study area, values from accuracy assessment over Bhutan...
Himalaya were considered. The value for error in $\sin \alpha$ was taken as $\pm 8.7\%$. The total uncertainty in ice volume estimated was 18% and the same was assumed for lake volume.

**Development of a semi-automated tool for potential future expansion of lakes**

The method discussed here is ideal for studying a few glaciers, but can be cumbersome when applied to a larger number of glaciers. The method was partially automated using Python script, which can be used to derive information about glacier depth and lake volume. The tool uses the ArcPy module available from ArcGIS 10.1 version and is executed via a graphical user interface (GUI) built using the Tkinter module in python. This is a multipurpose tool which gives estimates of glacier thickness and potential future expansion of glacier lakes. The volume of the lake and spatial distribution of lake depth provided by the tool can be useful for hydrodynamic modelling of outburst floods and impact assessments. This tool can be applied to any glaciers for which input data are available. It requires DEM, surface velocity, glacier boundary, contour polygons and flowlines as inputs. This tool uses a velocity and slope-based model to provide the fully distributed ice thickness and future lake depth using an automated workflow. With present knowledge on glacier lakes being limited, the automated tool has the potential for use in a large number of glaciers.

**Results and validation**

The surface velocity of ten glaciers was estimated using COSI-Corr from the satellite images of 2001 and 2002. The velocity data suggest that the highest mean velocity is 22 m/year in glacier no. 6 and the lowest mean velocity is 5 m/year in glacier no. 8. The mean velocity for all 10 glaciers along the flow line was estimated as 14 m/year. The ice thickness distribution has been estimated for the ten glaciers using laminar flow model. The maximum ice thickness was observed in Zemu glacier (glacier no. 2) as $439 \pm 57$ m and Figure 3 shows the spatial distribution of ice thickness. The maximum ice volume of $5.7 \pm 1$ km$^3$ was estimated for the same glacier (glacier no. 2) with an area of $69 \pm 3.4$ sq. km (Table 1). The total volume of the 10 glaciers in Tista Basin was estimated as $9.75 \pm 1.8$ km$^3$.

The bed topography of all the glaciers was estimated from the spatial distribution of glacier depth and surface topography. Subsequently, overdeepening of the lakes (in the ten glaciers) and their volumes were estimated (Figures 4 and 5c). However, no overdeepening was observed in the Zemu glacier (glacier no. 2). The total volume of the nine lakes was estimated as $149 \pm 26$ million m$^3$ in 2001 and $246 \pm 44$ million m$^3$ in 2015. Therefore, increase in volume of the lakes from 2001 to 2015 was $97 \pm 17$ million m$^3$, which included the formation of two new lakes near the terminus of glacier nos 3 and 5 (Figure 4). The lake near the terminus of Tista Khangse glacier
Overdeepening in all glaciers, excepts glacier nos 2 and 6. Further expansion of the four existing glacier lakes can be seen in glaciers nos 4, 6, 7 and 10. (glacier no. 10) showed maximum predicted depth of 279 m; it also showed maximum modelled volume of 150 million m$^3$ with an area of 2.2 sq. km.

The modelled depth of ice in the South Lhonak glacier was as high as 250 m in the accumulation area and 60 m in the ablation area, and bed topography distribution of the glacier was between 5006 and 7434 m asl. Satellite images of 2001 and 2015 suggest an expansion of the lake from 0.80 to 1.30 sq. km the this time interval (Figure 5a and b). In addition, the model suggests that it will further expand up to an area of 1.90 sq. km (Figure 5c). The modelled volume of the lake during 2015 was estimated as 60 million m$^3$. With further retreat of the glacier, the lake can grow to a maximum predicted volume of

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**Figure 4.** Overdeepening in all glaciers, excepts glacier nos 2 and 6. Further expansion of the four existing glacier lakes can be seen in glaciers nos 4, 6, 7 and 10.
Table 1. Area and volume estimates of glaciers and glacier lakes

| Number | Glacier Lake area | Glacier Lake volume |
|--------|------------------|---------------------|
|        | Area (km²) | Volume (km³) | Area (km² | Volume (km³) | Area (km²) | Volume (10⁶ m³) | Area (km² | Volume (10⁶ m³) | Area (km²) | Volume (10⁶ m³) |
| 1      | 2.5       | 0.2      | –        | –        | 0.05      | –        | –        | –        | –        | –        | –        |
| 2      | 69        | 5.7      | –        | –        | –        | –        | –        | –        | –        | –        | –        |
| 3      | 10        | 0.9      | –        | 0.5      | 0.9       | –        | –        | 40       | 60       | –        | –        |
| 4      | 3.5       | 0.15     | 0.2      | 0.35     | 0.7       | 7        | 10       | 20       | 20       | –        | –        |
| 5      | 11.5      | 0.6      | –        | 0.07     | 0.3       | 29       | 60       | 90       | 29       | 28       | 29       |
| 6      | 12        | 0.7      | 0.8      | 1.3      | 1.9       | 20       | 28       | 29       | 20       | 28       | 29       |
| 7      | 7         | 0.3      | 0.6      | 0.8      | 0.85      | 20       | 28       | 29       | 20       | 28       | 29       |
| 8      | 8         | 0.5      | –        | –        | 0.6       | –        | –        | 25       | –        | –        | –        |
| 9      | 5         | 0.3      | –        | –        | 0.3       | –        | –        | 10       | –        | –        | –        |
| 10     | 7.2       | 0.4      | 1.7      | 1.8      | 2.2       | 93       | 105      | 150      | 93       | 105      | 150      |

Figure 5. South Lhonak lake in (a) 2001 and (b) in 2015, including the extent of future prediction. (c) Predicted lake formation along with depth values.

90 million m³ (Table 1). The maximum and average depth of the lake when it reaches its maximum extent was estimated to be 170 ± 30.6 and 49 ± 8.8 m respectively.

Field observations based on surveys in 2014 and 2016 suggested that volume of the lake was 65.81 ± 3 million m³, which is close to the model-derived value of 60 ± 10.8 million m³. The difference may due to some uncertainties in the model and due to limitation of field instrument. The maximum depth of the lake from bathymetric survey was 131 ± 2.5 m, with an average depth of 67.05 ± 2.5 m and the model estimated maximum and average depth in 2015 was 160 ± 28.8 and 51.4 ± 9.3 m respectively. The area of the lake in 2015 was estimated as 1.3 ± 0.09 sq. km from the present model, which matches with the areal extent derived by Sharma et al. To further compare the model estimate, field measurements were compared with depth measurements of the lake derived from 2014 field survey data. The Hondex
Discussion and conclusion

In this study, volume of six existing glacier lakes has been calculated. This provides useful information to the scientific community, as it is difficult to obtain such data by conventional field methods due to remote location of the glacier lakes. It is an important step towards understanding the disaster potential of existing glacier lakes. Among these lakes, modelled results of the South Lhonak lake were compared with in situ observations. The modelled volume of the South Lhonak lake was validated with the echo sounder, and was observed to be within ~9% uncertainty relative to the volume derived by field measurements.

This indicates the usefulness of the present method in estimating area, depth and volume of moraine dammed lakes which are attached to glacier snouts. In addition, future expansion of the lake with volume of 90 million m$^3$ has been predicted. This large amount of water has the potential to cause disaster in downstream regions. The present study has shown large increases in water volume in the other glacier lakes also. The volume in individual glacier lakes varies from 15 to 150 million m$^3$. Therefore, major field studies are necessary to further understand the disaster potential. This study has also identified three new sites where lakes can form in future. The volume of such lakes is also large and ranges from 1 to 25 million m$^3$. Hence, further monitoring of these regions is necessary. The study presents an approach based on remote sensing data and models, which can provide unique information to planners so as to provide better safety to people living in the Himalaya.

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