The effects of functional diversity on biomass production, variability, and resilience of ecosystem functions in a tritrophic system

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Diverse communities can adjust their trait composition to altered environmental conditions, which may strongly influence their dynamics. Previous studies of trait-based models mainly considered only one or two trophic levels, whereas most natural systems are at least tritrophic. Therefore, we investigated how the addition of trait variation to each trophic level influences population and community dynamics in a tritrophic model. Examining the phase relationships between species of adjacent trophic levels informs about the strength of top-down or bottom-up control in non-steady-state situations. Phase relationships within a trophic level highlight compensatory dynamical patterns between functionally different species, which are responsible for dampening the community temporal variability. Furthermore, even without trait variation, our tritrophic model always exhibits regions with two alternative states with either weak or strong nutrient exploitation, and correspondingly low or high biomass production at the top level. However, adding trait variation increased the basin of attraction of the high-production state, and decreased the likelihood of a critical transition from the high- to the low-production state with no apparent early warning signals. Hence, our study shows that trait variation enhances resource use efficiency, production, stability, and resilience of entire food webs.

Functional diversity has proven to be important for linking community structure to ecosystem functions such as biomass production and resource use efficiency. Our understanding of the multifaceted impact of functional diversity on ecosystem functioning, and on the dynamics of populations and communities has been greatly advanced by adopting a trait-based point of view. In particular, functional traits link morphological, physiological or phenological features of a species to a certain community or ecosystem function. A prevalent example is simply body size, which is related to several functions such as growth (larger organisms tend to grow slower), prey preference (predators tend to be larger than their prey), or nutrient uptake (larger cells have higher nutrient demands). Trait-based models of simple food web modules have facilitated detailed mechanistic understanding of dynamics observed in the laboratory and in the field. For example, observed anti-phase predator-prey cycles between zooplankton and algae have been attributed to the co-occurrence of fast-growing undefended and slow-growing, well-defended prey phenotypes.

However, such trait-based models have mainly been restricted to describing trait variation on one or two trophic levels. Likewise, only up until recently, empirical studies on functional diversity have been limited to considering trait variation in only autotrophs (plants or algae), or both autotrophs and herbivores, with few exceptions. This strongly contrasts with the fact that natural food webs are in general complex multitrophic networks. Focusing only on direct, bitrophic predator-prey interactions neglects the intricate effects of more complex, partly indirect interactions spanning multiple trophic levels, such as trophic cascades. These multi-trophic effects may be very important factors affecting the relevant ecosystem functions. For instance, the total number of trophic levels may strongly influence the efficiency of nutrient exploitation. In addition, as predation is an important factor in many food webs, trait variation on the predator level is expected to have an important influence on ecosystem functioning. Hence, including additional trophic levels with functional diversity is a very natural step towards improving the accuracy and descriptive power of trait-based models.

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We developed a tritrophic model to study the effects of trait variation at all trophic levels on food web dynamics. Particularly, the dynamics of a simple tritrophic linear food chain will be compared to a tritrophic food web where prey species are either defended or undefended, and predator species are either selective or non-selective feeders. Trade-offs between these traits are explicitly built in such that defended prey have a lower growth rate, and selective feeders have a lower half-saturation constant to allow for efficient feeding at low prey densities. Our model structure allows for a gradual increase of the trait differences between the species at each trophic level, from a simple linear chain up to a fully separated food web with maximal trait differences. As the trait differences increase, the species will fulfill increasingly different functions; in this way, we are able to link trait differences to functional diversity.

We use the tritrophic model to investigate how an increasing degree of trait variation affects:

- the production of the system;
- the efficiency of the energy transfer towards the higher trophic levels;
- the temporal biomass variability at the population and community level; and
- the dynamic properties and the resilience of alternative stable system states.

Our results provide theoretical evidence that trait variation has a significant impact on all of these properties. To the best of our knowledge, we present the first systematic, multi-trophic study which mechanistically explains such patterns and explicitly discusses their relevance to ecosystem functions and stability.

**Methods**

We developed a tritrophic model where basal species are consumed by intermediate species, which in turn are consumed by top species. The species biomass densities are denoted by $B$, $I$, and $T$, respectively. In addition, the uptake of a limiting nutrient with concentration $N$ (in this case nitrogen) by the basal species is modeled explicitly. We assume a chemostat environment, which causes all nutrients and biomass of species to be washed out at a constant rate, $\delta$, the dilution rate. The washed out volume is replaced by new medium rich in nutrients.

**Model equations.** As in, we include two relevant functional traits. The prey species $B$ and $I$ may be defended against predation: specifically, there will be defended (d) and undefended (u) species. Investing in a defense strategy requires sacrificing a certain amount of resources which could have otherwise been put into growth. Hence, the defended species have a lower growth rate than the undefended species, but are rewarded by being insusceptible to certain consumers. The consumer species $I$ and $T$ are able to specialize feeding on a certain prey species, leading to selective (s) and non-selective (n) species. Here, the non-selective consumer species consume all species on the trophic level below. In contrast, the selective species are only able to consume the undefended prey species, but they are able to exploit low food densities at a higher rate, reflected in a lower half-saturation constant.
Representing each possible trait combination on all trophic levels by one species leads to a food web with two basal species, four intermediate species and two top species (Fig. 1c). In order to write down the equations compactly, the following equivalence is explicitly stated:

\[ B^u \equiv B_1, \quad B^d \equiv B_2, \quad I^u_1 \equiv I_1, \quad I^d_1 \equiv I_2 \]

\[ I^u_{\nu} \equiv I_{\nu}, \quad I^d_{\nu} \equiv I_{\nu}, \quad T_s \equiv T_1, \quad T_n \equiv T_2. \]

In their most general form, the equations used have the following shape:

\[
\begin{align*}
N &= \delta(N_0 - N) - \zeta \sum_i r_i B_i \\
\dot{B}_i &= r_i B_i - \sum_j s_{ij} l_j - \delta B_i \\
\dot{l}_j &= e \sum_i s_{ij} l_i - \sum_i \gamma_{ij} T_i - \delta l_j \\
\dot{T}_i &= e \sum_j \gamma_{ji} T_i - \delta T_i
\end{align*}
\]

(3)

with \( i \in \{1, 2\}, j \in \{1, 2, 3, 4\}\), where \( N_0 \) denotes the incoming nutrient concentration. Following typical experimental conditions, we assume nitrogen as the limiting nutrient (N). Hence, the nutrients are measured in nitrogen concentration, as compared to carbon for biomass, therefore, the nitrogen-to-carbon weight ratio \( c_N/c_C \) is required to scale the basal \( (B_i) \) growth terms. Moreover, the basal growth rate \( r_i \) is described by a Monod function, with maximum growth rate \( r'_i \) and a nutrient-uptake half-saturation constant \( h_N \). The intermediate and top species have a generalized Holling-type-III functional response, with maximum growth rates \( g'_j \) and \( \gamma'_i \), half-saturation constants \( M \) and \( \mu \), and Hill coefficients \( h \) and \( \eta \), respectively. This means:

\[ r_i = r'_i \frac{N}{N + h_N} \]

(4)

\[ g_{ij} = g'_j \frac{(p_{ij} B_j)^h}{\sum_l (p_{ij} B_j)^h + 1} \]

(5)

\[ \gamma_{ji} = \gamma'_i \frac{(p_{ji} l_i)^\eta}{\sum_l (p_{ji} l_i)^\eta + 1} \]

(6)

and,

\[
\begin{pmatrix}
B^u \\ B^d
\end{pmatrix} = \begin{pmatrix}
\frac{1}{M_{u,s}} & \frac{1}{M_{u,d}} \\
\frac{1}{M_{d,s}} & \frac{1}{M_{d,d}}
\end{pmatrix}
\begin{pmatrix}
I^u_s \\ I^d_s
\end{pmatrix}, \quad \phi = \begin{pmatrix}
\frac{1}{\mu_{u,s}} & \frac{1}{\mu_{d,s}} \\
\frac{1}{\mu_{u,d}} & \frac{1}{\mu_{d,d}}
\end{pmatrix}
\begin{pmatrix}
T_s \\ T_n
\end{pmatrix}
\]

(7)

such that e.g. \( M_{u,s} \) indicates the half saturation constant of the undefended species being grazed by the selective species, etc.

Finally, our model includes a parameter, \( \Delta \), which explicitly controls the species' trait values. Abstract traits such as defense and selectivity are linked to concrete and measurable parameters describing the species' interactions. For the basal species, their maximal growth rate \( r'_i \) is linked to their position on the defense axis (Fig. 1d). The intermediate species have two trait values: defense is again linked to their maximal growth rate \( e \cdot g'_j \), and the half saturation constant \( M_{ij} \) is determined by their degree of selectivity; both of these traits affect the overall growth rate of the intermediate consumers. The top species have only one trait, selectivity, which is linked to their half saturation constant \( \mu_i \). As will be shown below, the equations are parametrized in a way such that for \( \Delta = 0 \) the linear chain system, where all species per trophic level are functionally identical, will be described (Fig. 1a). As \( \Delta \) is increased, the system changes in a continuous way, where some prey species gradually become more and more defended (Fig. 1b), such that they can be preyed on less and less by the selective species. In addition, the selective species are gradually able to feed more efficiently on the undefended species. Finally, for \( \Delta = 1 \) the trait differences are maximal, as is the case in Fig. 1c: the selective species do not feed on the defended prey anymore.
Table 1. Standard parameter values used in this study when the trait differences are maximal, i.e., \( \Delta = 1 \).  

| Parameter                                | Value               |
|------------------------------------------|---------------------|
| Body mass ratio between adjacent trophic levels | \( m_I/m_B = m_2/m_1 = 10^3 \) |
| Allometric scaling exponent \( \lambda \) | \( -0.15 \)          |
| Inflow nutrient concentration \( N_c \)  | \( 1120 \mu gN/l \) |
| Dilution rate \( \delta \)                | \( 0.055 \)          |
| Nutrient half-saturation const. of \( B \) | \( h_b = 10 \mu gN/l \) |
| Nitrogen to carbon ratio of \( B \) \( c_B/c_C \) | \( 0.175 \)          |
| \( B^1 \) max. growth rate \( r'_1 \)    | \( 1/day \)          |
| \( B^1 \) max. growth rate \( r'_2 \)    | \( 0.66/day \)       |
| Conversion efficiency \( \epsilon \)      | \( 0.33 \)           |
| \( P^1 \) max. grazing rate \( g'_{1,s} \) | \( 1.08/day \)       |
| \( P^1 \) max. grazing rate \( g'_{1,d} \) | \( 0.70/day \)       |
| \( T^1 \) half-saturation const. \( M_{1,s} \) | \( 300 \mu gC/l \)   |
| \( T^1 \) half-saturation const. \( M_{1,d} \) | \( 800 \mu gC/l \)   |
| \( T^1 \) conversion efficiency \( \epsilon \) | \( 0.33 \)           |
| \( T^1 \) max. grazing rate \( g'_{1,s} \) | \( 0.38/day \)       |
| \( T^1 \) half-saturation const. \( \mu_1 \) | \( M_{1,s} = 300 \mu gC/l \) |
| \( T^1 \) half-saturation const. \( \mu_3 \) | \( M_{1,s} = 800 \mu gC/l \) |

The parameter values are set to vary logarithmically with \( \Delta \). This implies that parameter changes occur proportional to the starting value in both directions, since \( r'_i \) and \( g'_{i,d} \) appear as linear factors in the differential equations. For consistency, the elements of \( p \) and \( \varphi \) are also varied logarithmically. Concretely, this means that:

\[
\log \left( \theta(\Delta) \right) = \log \theta_0 + \Delta \cdot (\log \theta_1 - \log \theta_0)
\]

where \( \theta \) is \( r'_a \), \( r'_d \), \( g'_{a,d} \) or any of \( p_j \) or \( \phi_j \). In this way, \( \Delta = 0 \) implies \( \theta = \theta_0 \) such that all the trait values are equal in the following manner:

\[
r'_d(\Delta = 0) = r'_o = r'_d(\Delta = 0),
\]

\[
g'_{a,d}(\Delta = 0) = g'_{o,d} = g'_{a,d}(\Delta = 0),
\]

\[
\frac{1}{M_{a,n}}(\Delta = 0) = \frac{1}{M_{b}} = \frac{1}{M_{a,n}}(\Delta = 0),
\]

and similarly for the other elements of \( p \) or \( \varphi \). We define the parameter values \( \theta_0 \) of the \( \Delta = 0 \) system as arithmetic averages of the extreme values \( \theta_i \) in the \( \Delta = 1 \) system, on a logarithmic scale, e.g.:

\[
\log r'_a = \frac{\log \left( r'_a(\Delta = 1) \right) + \log \left( r'_a(\Delta = 1) \right)}{2},
\]

and similarly for the other parameters. These extreme values are shown in Table 1.

As the logarithm of 0 is undefined, this requires the elements of \( p \) and \( \varphi \) related to the defended-selective species’ interactions for \( \Delta = 1 \) to be nonzero. In this case \( 10^{-4} \) was taken, which is low enough not to affect our results (see Fig. A1, Appendix A). Note also that the set of 9 equations in equation (3), when the species on each trophic level are exactly equal (\( \Delta = 0 \)), is mathematically equivalent to a linear chain system with 4 equations, up to a slight parameter transformation. Specifically, the 9-equation food web system corresponds to a 4-equation food chain by setting \( M \rightarrow 2^{(h-1)/h}M \) and \( \mu \rightarrow 4^{(h-1)/h} \mu \). For details of the derivation, see Appendix B.

**Model parametrization and analysis.** In order to decrease the number of free parameters, and simultaneously increase the realism of the model, the species’ growth rates were scaled allometrically to their body mass

\[
\text{intermediate growth rate} = \frac{m_I}{m_B} \mu
\]

with body masses \( m \) and the exponent \( \lambda \) given typical for planktonic systems (Table 1). The same relationship holds true for the ratio between the maximum growth rates of the intermediate and the top species.

This model was developed as a chemostat model, with an eye towards potential experimental application. Chemostat experiments have been very successful in identifying and understanding ecological and evolutionary interactions of planktonic systems, and many other microbiological systems. In such experiments, many factors influencing dynamics in question, such as nutrient supply, light supply, temperature, etc., are kept constant and/or closely monitored. This procedure greatly facilitates observation of the interactions of interest between species in the chemostat. For this reason, extra care was taken to have empirically motivated and realistic values of
the remaining model parameter values (Table 1). Specifically, the parameter values we use are representative for planktonic chemostats. However, this does not mean that our results apply only to planktonic systems. In fact, as we show in Appendix A, similar results are obtained when the model parametrization is more adapted towards terrestrial food webs, for example.

To get a better understanding of how much certain values of $\Delta$ sets the species on the three trophic levels apart, we here consider a few exemplary cases. At $\Delta = 0$, the varied parameters are identical (and so are the species), while at $\Delta = 0.2$, maximal growth and grazing rates of the undefended species are 9% higher than those of defended species, and half saturation constants of non-selective species are 15% higher than selective species. At $\Delta = 0.5$, the differences are 23% and 42%, respectively; at $\Delta = 1$ they are 50 and 100%.

For simplicity and to reduce the dimensionality of the system somewhat, in the rest of the text it will be assumed that

$$h = \eta, \quad M = \mu. \quad (14)$$

Hence, $h$ will denote the Hill exponent, and $M$ the half-saturation constant, of the functional response between both the first and the second, and between the second and the third trophic level. Additional narrowing of parameter ranges was achieved by requiring coexistence of the species in both the chain and the maximally separated food web. More information on the size of the range for which all species are able to coexist, as well as generalizations of our results for different model structures can be found in Appendix A.

To characterize the differences between the different attractors, the different phase relationships between predator-prey pairs were investigated. These phase relationships were obtained by calculating the Discrete Fourier Transform (DFT) of the simulated time series. Due to the non-sinusoid shape of the biomass oscillations, a signal with only a single frequency will generate an infinite amount of peaks in the frequency spectrum. These are necessarily multiples of the original frequency $f$, and the height of the peaks will scale as $1/f^n$. This means they are easily identified in the frequency spectra when shown on a log-scale, by the linear decay in peak height.

The solutions of the differential equations presented were obtained numerically in C using the SUNDIALS CVODE solver\(^43\), with relative and absolute tolerances of $10^{-10}$. Output data were studied using Python and several Python packages; in particular NumPy, SciPy and Matplotlib\(^44,45\).

**Results**

Firstly, we compare the biomass dynamics of the linear chain to the dynamics of the maximally trait-separated food web, where trait differences within each trophic level are maximal. Secondly, we study certain properties of the system, such as the temporal variability of population and community biomasses, and the relative abundances of species, while gradually increasing the amount of standing trait variation at each trophic level from a linear food chain to the maximally trait-separated food web.

The amount of trait variation is described by $\Delta$ ranging continuously from 0 to 1. When $\Delta = 0$ we describe the linear chain without trait variation, and when $\Delta = 1$ we describe the maximally trait-separated food web. This fully separated food web consists of defended and undefended prey species, which are being preyed upon by non-selective and/or selective predator species (Fig. 1c). The benefits and costs of the different offense-defense strategies are linked to each other through predefined trade-offs (see Methods). The defended species have a lower growth rate than the undefended species, but in turn, they are not preyed upon by the selective species of the next trophic level in the fully separated web. Similarly, the selective species, while unable to prey on the defended species, are able to graze the undefended species more efficiently at low prey concentrations than their non-selective counterparts.

Our results are first summarized schematically in Fig. 2, subsequent mechanistic details are presented in the sections and figures below. We observe two alternative stable states with low vs. high total production (State 1 and 2 in Fig. 2) in both the linear chain (low trait variation) and the maximally separated food web (high trait variation). In the low-production state, the high mean concentration of free nutrients corresponds to a low amount of total biomass and consequently, a low total production. In the high-production state, in contrast, the low mean nutrient concentration implies that most of the nutrients are stored in the biomass which implies a high total production. Note that at equilibrium, the total amount of nutrients in the system is always constant because the chemostat model’s dilution rate $\delta$ is constant for all species.

In the food chain without trait variation (left part of the biomass pyramids in Fig. 2), the population-level biomass dynamics for the low-production state (Fig. 3a) exhibit pronounced predator-prey cycles, while the high-production state exhibits slower cycles with lower amplitudes (Fig. 3b). The respective phase relationships of these oscillations (right part in Figs 2 and 3c,d) may inform about the ecological mechanism behind the two different states (for details, see section 3.1). In the low-production state, fast cycles with high amplitudes occur due to the strong coupling between adjacent trophic levels. Such a strong interaction between predators and their prey is indicated by the quarter-cycle phase lags (henceforth referred to as $\frac{1}{4}$-lag cycles) (Fig. 3c). In the high-production state the top and intermediate level still exhibit $\frac{1}{4}$-lag cycles, but the phase difference between the intermediate and basal level is significantly larger (Fig. 3d). This offset in the phase-relationship indicates that the top-down control over the intermediate level is so strong in the high-production state that the intermediate level’s dynamics are less closely coupled to the basal level than in the low-production state. The basal level is then free to fully exploit the available nutrients.

The decoupling of the intermediate and basal level results in a lower temporal variability, especially at the basal level, and hence, reduces times of strong basal suppression during which the nutrients can almost reach their capacity as observed in the low-production state. In the high-production state, the overall higher primary production combined with the lower temporal variability between the basal and the intermediate level enhances the energy transfer through the food chain and results in a top-heavy biomass pyramid.
When the food chain becomes a food web by adding trait variation (right part of the biomass pyramids in Fig. 2), the biomass dynamics of the low-production (Fig. 4a) and high-production state (Fig. 4b) as well as their respective phase-relationships (Fig. 4c–f) become more complex because a slow and a fast timescale underlie the oscillations (see Section 3.1 for details). The phase differences between predators and their prey inform about the intensity of top-down control in the system as indicated by arrow width in (a), i.e. ¼-lag cycles indicate strong coupling between predator and prey. (c) Within trophic level out-of-phase cycles indicate compensatory dynamical patterns, where the different species exploit different temporal niches, and hence, reduce the community temporal variability.

Figure 2. Schematic overview of our results. (a) The model system (with $B$ basal species, $I$ intermediate consumers and $T$ top predators) always exhibits two alternative stable states, State 1 (low-production) and 2 (high-production), for both low and high amounts of trait variation. As trait variation is added, the system tends toward the high-production state with the top-heavy biomass pyramid (solidly drawn states have a larger basin of attraction than grayed out states). (b) The phase differences between predators and their prey inform about the intensity of top-down control in the system as indicated by arrow width in (a), i.e. ¼-lag cycles indicate strong coupling between predator and prey. (c) Within trophic level out-of-phase cycles indicate compensatory dynamical patterns, where the different species exploit different temporal niches, and hence, reduce the community temporal variability.

Figure 3. Biomass and nutrient dynamics on the two different states for the tritrophic chain for $h = 1.1 (\eta)$, and their corresponding phase relationships. ($N =$ nutrients, $B =$ basal species, $I =$ intermediate species and $T =$ top species). The relative phases of the low-production state shown in (a) (mean nutrient level $\approx 250 \mu g N/l$) are plotted in panel (c). The phases of the high-production state shown in (b) (mean nutrient level $\approx 10 \mu g N/l$) are plotted in panel (d). In both cases the phases relative to the top species are shown.

When the food chain becomes a food web by adding trait variation (right part of the biomass pyramids in Fig. 2), the biomass dynamics of the low-production (Fig. 4a) and high-production state (Fig. 4b) as well as their respective phase-relationships (Fig. 4c–f) become more complex because a slow and a fast timescale underlie the oscillations (see Section 3.1 for details). Information regarding intensity of top-down control is only deduced from the phase-relationships of the oscillatory mode that explains most of the observed variation, i.e. the fast timescale of the low-production state (Fig. 4d) and the slow timescale of the high-production state (Fig. 4e). Similar to the food chain without trait variation, the strong top-down control by the top level and subsequently, the decoupling of the intermediate and basal level in the high production state again results in lower temporal variability, a temporally more balanced nutrient use, and a more efficient energy transfer towards the top level. Importantly, the high-production state becomes more likely than the low-production state with increasing trait
variation, i.e., its basin of attraction increases, making it more resilient against external disturbances (for details, see Fig. 5 and Section 3.2).

As trait variation ($\Delta$) increases, selective and non-selective consumers at the top level exploit different temporal niches and force the intermediate level to split up into two distinct groups comprising the defended and the undefended species, respectively. As both groups include both selective and non-selective consumers, this further weakens the interaction between the intermediate and basal levels, strengthening the aforementioned mechanisms that stabilize the high-production state. Notably, the mean population biomasses stay relatively constant as trait variation increases (cf. Fig. 6c,d), while the community temporal variability decreases (Fig. 6e,f, gray lines). This effect could also be predicted from the phase relationship diagrams, which show that with increasing...
trait variation, competing species within the same trophic level move out-of-phase with each other (Fig. 4c,e,f). Such out-of-phase cycles indicate compensatory dynamical patterns with potentially high amplitudes at the population level. However, because the different species are able to exploit different temporal niches, the community temporal variability is kept low.

In summary, adding trait variation safeguards the high-production state which is characterized by a high top-level biomass resulting from an efficient transfer of energy towards the higher trophic levels, and low temporal variability due to weak coupling between the intermediate and basal levels and prominent compensatory dynamics within the lower trophic levels. Contrarily, losing trait variation increases the risk of an irreversible transition to the low-production state, which is characterized by a lower top-level biomass resulting from the less efficient transfer of energy towards the higher trophic levels, and higher temporal variability. With trait variation added, primary production increases from the low- to the high production state by a factor of 1.5 and the efficiency of the energy transfer towards the top level increases by a factor of 2 (See Table C1 in Appendix C). Hence, adding trait variation results in a more productive and energy-efficient food web.

More details about the above-mentioned results are presented in the respective sections below.

Phase relationships as a way to identify underlying mechanisms. In order to understand how to use the phase relationships between different populations of a complex food web, such as the maximally trait-separated web (Fig. 1c), to uncover the mechanisms driving their dynamics, let us first look at the simpler linear chain containing only three species (Fig. 1a). As mentioned above, the state shown in Fig. 3a with a
mean nutrient concentration of about 250 μgN/l will be called the low-production state, relative to the other state (Fig. 3b) which has a much lower mean nutrient concentration of around 10 μgN/l and therefore will be called the high-production state.

Closer inspection of the time series reveals the origin of the difference in mean free nutrient levels between the two states. In the low-production state (Fig. 3a) the intermediate level is able to grow to sufficiently high densities to graze the bottom level down significantly, despite the predation pressure imposed by the top species. Hence, the nutrient uptake is strongly reduced for a considerable amount of time leading to a relatively high mean nutrient level. Conversely, in the high-production state (Fig. 3b), the higher biomass at the top level implies a stronger grazing pressure on the intermediate level. The intermediate species are thus not able to grow to the density levels reached on the low-production state, and in turn, do not graze the basal level down to low densities. Hence, the mean nutrient level is much lower. Here, we define top-down effects simply as effects arising from the terms linking a species to the trophic level above it, and vice-versa for bottom-up effects. In this way, increased grazing pressure constitutes an increase in top-down control.

Using this definition, we could conclude that the overall control exerted by the top level is higher in the high-production state than on the low-production state. Such an observation cannot be made as straightforwardly by inspecting only the mean biomass levels, as the temporal averages of the intermediate and basal biomasses are quite similar in both states and thus, they do not inform about potential changes in the production at each level. Therefore, examining the degree of top-down or bottom-up control in the case of non-static dynamics requires information about the oscillations themselves.

Interestingly, the phase differences between the different trophic levels contain sufficient information to reach the same conclusions regarding the strength of top-down control in the two states. In the low-production state, the phase differences between the top and intermediate level, and the intermediate and bottom level, are about a ¼-cycle (Fig. 3c), reflecting the presence of clear predator-prey oscillations, i.e., cyclic change between top-down and bottom-up control, between both the top and intermediate level, and the intermediate and basal level. In contrast, in the high-production state, the phase lag between the intermediate and basal level is significantly more than a ¼-cycle (Fig. 3d), indicating rather weak interactions between these two different trophic levels.

With this in mind, we now investigate the fully trait-separated food web (Δ = 1, Fig. 1c), whose dynamics are shown in Fig. 4a,b. Just as the linear chain, the system settles down to a stable limit cycle. While the dynamics are visually much more complex when compared to the linear chain, the basic properties and differences between the two states remain the same. However, in contrast to the chain, the discrete Fourier frequency spectra (cf. Appendix C, Fig. C3) reveal two distinct frequencies at substantially different timescales. Despite this increase in complexity, our results clearly show that the phase relationships between distinct populations of adjacent trophic levels provide substantial information about the regulations of trophic interactions and changes therein. The absence of qualitatively different interaction types (e.g., omnivory) allows us to meaningfully compare the phase relationship between each individual predator-prey pair in our trait-separated food web to its expected value in isolation.

The low-production state of the maximally separated food web (Fig. 4a) exhibits two important timescales governing the overall dynamics. First, the same high-frequency oscillations as were observed for the food chain are present, with the ¼-lag cycles indicative of predator-prey oscillations (Fig. 4d). Second, oscillations on a slower timescale are found. Their phase relationships show that they arise from the trait differences between species (Fig. 4c). Here, the top species are almost completely out of phase relative to each other. Consider first the selective predator T, which preys only on the undefended intermediate species I and I. The phase relationship diagram shows that these species precede T by the regular ¼-lag. The same is true for T, which is preceded by a quarter-cycle by the deflected intermediate species I and I. Quarter-lag cycles are not observed between the basal and intermediate trophic level, which indicates that the trait differences within the top trophic level influence the intermediate level more strongly as those on the intermediate level influence the basal level. As the two alternating groups of defended and undefended intermediate species contain a selective and non-selective grazer on the basal species, they exert together approximately the same grazing pressure on both types of basal species. Consequently, no clear phase relationship between the intermediate and basal level is found. However, visual inspection combined with analysis of the Discrete Fourier Transform (DFT) spectrum (Appendix C, Fig. C3) shows that the high-frequency component is the dominant one, explaining most of the observed variation in the biomass. Hence, the biomass dynamics reflect an overall balance between top-down and bottom-up interactions in the low-production state, similar to the simple linear chain.

In the high-production state of the maximally separated food web (Fig. 4b), the dynamics in comparison to the linear chain is even more pronounced. The basal species exhibit a clear compensatory dynamical pattern, with alternating biomass peaks of defended and undefended species. While the dynamics appear highly irregular, the frequency spectrum shows that they are also mainly driven by two frequencies. On the lower of these frequencies, which explains most of the variation observed in this state, the phase relationships resemble those of the low frequency in the low-production state (Fig. 4e vs. 4c), with the exception of the basal species, which now cycle out of phase. The selective and non-selective top species also move out of phase, which leads the groups of defended and undefended intermediate species to behave similarly, as they each precede their respective main predator. As in the low-production state, no further relationship can be identified between the intermediate and the basal level.

However, the high frequency roughly corresponding to that of the chain also has an influential component in the Fourier spectrum. On this frequency, the phase relationships show that the basal species also move out-of-phase. In contrast to the dominant lower frequency, the intermediate species are now split into two groups according to their main prey type. The non-selective intermediate species follow the defended basal species, and the selective intermediate species the undefended basal species, by a ¼-lag. As each of these two groups...
of intermediate species contains both a defended and undefended type, no further relationship can be drawn between the phases of the intermediate and the top level.

In summary, the strength of top-down control across trophic levels may be inferred from the phase relationships in both the linear chain and the maximally separated food web. The phase-relationships further reveal compensatory dynamics within trophic levels in the fully separated web.

**Trait variation increases resilience of the high-production state.** Recall that trait differences between the modeled species at each trophic level, determined by \( \Delta \) (equation (8)), can be varied continuously. Varying \( \Delta \) between \( \Delta = 0 \) (chain) and \( \Delta = 1 \) (maximally separated web) reveals the intermediate region between the two extremes considered so far.

In this intermediate region, the food web is not yet completely separated as is the case for Fig. 1c, although there are already trait differences between different species at each trophic level. That is, the selective predator species are not yet fully specialized: they are still able to prey on the defended species albeit with a lower efficiency than the undefended species. Accordingly, the undefended species are not fully defended against the selective predators. The difference in growth rates between defended and undefended species is thus gradually increased to its maximum value, which is obtained when \( \Delta = 1 \). In this way the trade-offs between defense and growth rate, and between selectivity and prey grazing efficiency, are explicitly built into the model.

To investigate the effect of trait variation on the likelihood of the system adopting either of the two alternative stable states, we determined the size of the basin of attraction of the high-production state. Figure 5 shows the relative frequency of a random initial value falling in this basin of attraction, as \( \Delta \) is varied. The random initial values were sampled from the set of all potentially accessible biomass configurations of the chemostat system, i.e., the total carbon content in the system does not exceed the maximum possible carbon content attainable by the incoming nutrient concentration \( N_c \).

The region of intermediate frequency values confirms that the bistability is an important aspect of the system. The typical behavior when varying \( \Delta \) from 0 to 1 is an increasing probability of reaching the high-production state. Furthermore, the graph shows an important dependency on the predator-prey functional responses' Hill coefficient \( h \): increasing the exponent also increases the probability of reaching the high-production state. Investigating the effect of other model parameters on the presence of bistability reveals that it is quite common for this type of model structure, and that the trends presented here are not limited to this particular part of the parameter space. For details, see Appendix A.

Over the whole range of \( \Delta \), there is a very sharp transition between the region where only the high-production state exists (dark blue), and the region where both states exist, indicated by the white dashed line (Fig. 5). Notably, the border decreases steeply as the trait difference \( \Delta \) is increased, indicating the much lower dependence on low-density grazing suppression for higher amounts of standing trait variation. The sharp border between the two regions is an indication that the low-production state undergoes a catastrophic bifurcation, where it suddenly disappears. Similar behavior is observed for the high-production state, indicated by the black dashed line. This transition is of particular ecological interest as it implies the sudden disappearance of the high-production, low-temporally-variable state. The region for \( h < 1.04 \) was not considered, as the amount of extinctions was too high. However, the graph indicates that the probability of reaching the high-production state decreases further.

**Dynamical properties of the alternative stable states under gradual changes in trait variation.**

Consider now \( h = 1.05 \) as a representative value capturing the most complex region in Fig. 5, to study the possible effects of varying \( \Delta \) on the system's dynamics. In this case, the low-production state exists over the whole range of \( \Delta \), its bifurcation diagram for the defended basal species \( B^d \) is shown in Fig. 6a. The qualitative features of the diagram are representative for the other species in the network, whose bifurcation diagrams are shown in Appendix C, Figs. C1 and C2.

For \( \Delta = 0 \), the oscillations are simple, in the sense that they are governed by a single timescale and have a constant amplitude, as the maxima and respectively minima each fall on the same position. As \( \Delta \) increases, this situation remains unchanged, up until the species become different enough for the second timescale to emerge, in which they exhibit a compensatory dynamical pattern. This explains the variation of the values of the extrema as the two timescales interact destructively and constructively.

The mean biomasses of the species (Fig. 6c) reveal that the selective top predator goes extinct for low values of \( \Delta \). In this case, the species are too similar to stably coexist due to a lack of niche differences, and the non-selective predator outcompetes the selective species. However, it quickly recovers as \( \Delta \) is increased and the species become more different. While this event causes some disturbances in the mean biomasses of the other species, outside of this range the values are more or less constant.

Disregarding the initial region of \( \Delta \) where the selective top predator goes extinct, all species’ \( CV \) exhibit a gradual decrease as \( \Delta \) is increased, up to the point where the second timescale enters the system (Fig. 6e). At this point, a sharp increase is observed as the complexity is enhanced by the interaction of the two timescales. The black to gray lines, depicting the \( CV \) of the biomasses at each trophic level as a whole, show that the sharp increase is not present on the trophic-level-scale. Hence, the increase in \( CV \) for each of the species can be solely attributed to the introduction of the second, slower timescale. As discussed above, species with different traits may move out of phase on this timescale, and thus the effects of the slower timescale on the temporal variability for the trophic level as a whole cancel out.

The bifurcation diagram for the high-production attractor (Fig. 6b) does not cover the full range of \( 0 \leq \Delta \leq 1 \) for \( h = 1.05 \), as it only exists on the right side of the black dashed line in Fig. 5. Furthermore, the attractor exhibits a much richer structure as \( \Delta \) is varied than the low-production attractor. Multiple bifurcations occur in which the dynamics are altered. In particular, lowering \( \Delta \) sufficiently the system undergoes a series of period-doubling bifurcations which lead to chaotic dynamics. Eventually the attractor undergoes a boundary crisis, as indicated by
both the sudden disappearance of the then chaotic attractor and the presence of a chaotic transient (Appendix C, Fig. C4).

The species’ mean biomass on the high-production state (Fig. 6d) reveal a similar monotonicity as those on the low-production state (Fig. 6c). A notable observation is the very low mean nutrient level along the whole range of $\Delta$. The nutrients show a very high CV (Fig. 6f), which can be attributed to their low mean value. In addition, the CV for each of the species is higher on the right side of the Hopf-bifurcations (higher $\Delta$), as compared to the left side for lower values of $\Delta$. However, just as for the low-production state, these increases are buffered when looking at the temporal variability of the trophic levels as a whole (black to gray lines). This reflects the compensatory dynamical pattern of the high-production state, where some of the species move out of phase, which leads to a reduction in temporal variability on the entire trophic level.

**Discussion**

We developed a generic tritrophic model to investigate the effect of varying degrees of trait variation on the dynamics of multitrophic food webs and their associated ecosystem functions such as the mean resource use efficiency, biomass production, temporal variability and resilience. By increasing the trait difference parameter $\Delta$ from 0, the system increases in complexity while it changes gradually from a simple chain without trait variation to a complex web with selective and non-selective consumers, and correspondingly defended and undefended prey. The relevant parameters affecting these traits (growth rate, edibility, food preference, and half saturation constant) are closely linked to the functions of the individual species in the food web. Hence, increasing $\Delta$ also increases the functional differences between the species, and thus, the functional diversity of the system. For $\Delta > 0$ but low, the trait differences are small which means the species are very similar, hence, the functional diversity at each trophic level is low. Correspondingly, for $\Delta$ close to one, the functional diversity of the system is high, even though the number of species is kept constant. Therefore, varying $\Delta$ is a means to study the effects of changing functional diversity on all three trophic levels on the dynamics of the whole system without potentially confounding effects of changing the number of species. The different aspects of how trait variation impacts the food web dynamics are discussed in detail below.

**Phase relationships help unravel complex trophic interactions.** Traditionally, effects of multi-trophic interactions such as trophic cascades and the degree of bottom-up or top-down control were studied using a rigid linear chain in equilibrium. However, natural systems are usually not simple chains, but highly complex webs with functionally diverse species at all trophic levels. Moreover, their dynamics may not evolve towards an equilibrium fixed point, but rather to a limit cycle, or a strange attractor where they will perpetually exhibit oscillatory behavior. This phenomenon can be separated from stochastic noise and has been observed in natural communities. Such oscillatory behavior gives rise to certain phase relationships between the biomass dynamics of the different species.

Additionally, in the maximally trait-separated food web (Fig. 1c), calculation of the Discrete Fourier Spectrum clearly exposes the two timescales at which major driving mechanisms take place. The emergence of a second timescale does not rely on the addition of a third trophic level as this feature has already been found in bitrophic systems showing that reduced top-down control may result in an increased phase difference between predator and prey. The relevant parameters affecting these traits (growth rate, edibility, food preference, and half saturation constant) are closely linked to the functions of the individual species in the food web. Hence, increasing $\Delta$ also increases the functional differences between the species, and thus, the functional diversity of the system. For $\Delta > 0$ but low, the trait differences are small which means the species are very similar, hence, the functional diversity at each trophic level is low. Correspondingly, for $\Delta$ close to one, the functional diversity of the system is high, even though the number of species is kept constant. Therefore, varying $\Delta$ is a means to study the effects of changing functional diversity on all three trophic levels on the dynamics of the whole system without potentially confounding effects of changing the number of species. The different aspects of how trait variation impacts the food web dynamics are discussed in detail below.

**Strength of trophic interactions.** We found that the main dynamical differences between the two alternative stable states present in our system can be explained by an increased top-down control of the top level on the intermediate level. When the intermediate level is strongly controlled, such as is the case on the high-production state, its species are unable to control the basal level. The basal level is in turn able to fully exploit the available nutrients, increasing the overall production in the system (See Appendix C, Table C1).

This result holds independent of the amount of trait variation present, and is in line with previous studies showing that reduced top-down control may result in an increased phase difference between predator and prey. Importantly, the larger than $\frac{1}{4}$-cycle phase difference between the basal prey and intermediate predator observed in our system with only one species per trophic level (Fig. 1a) shows that the common conception of anti-phase cycles as a ‘smoking gun’ for the presence of evolution, or other mechanisms causing trait changes does not hold any longer when considering multitrophic systems in which the intermediate predator faces strong top-down control by the top predator.

**Role of compensatory dynamics.** When a community consists of functionally diverse populations, a decline in one functional group can be accompanied by an increase of another. In this way, even though the individual populations exhibit high temporal variability in their biomasses in our model, the variability of the community biomass per trophic level remains low (Fig. 6f). Such an effect has been observed before in studies investigating the effect of standing trait variation or phenotypic plasticity on population dynamics. Hence, compensatory dynamics can be understood as a mechanism by which ecosystem functions such as biomass production can stay rather constant while individual populations may be highly variable. Compensatory dynamics are observed in both the high- and low-production state, for sufficiently high $\Delta$ (Fig. 4a,b). When present, they effectively decrease the biomass CV of the trophic level as whole, even though the CVs of the species’ individual biomass may be relatively high (Fig. 6c,f). These compensatory dynamical patterns naturally keep species within a trophic level moving out-of-phase relative to each other, and thus, can also be inferred by analyzing phase relationship diagrams.

Notably, the compensatory dynamics on the low-production state are only present at the slower timescale related to the trait dynamics (Fig. 4c). The dominant faster timescale does not exhibit compensatory dynamics.
by eutrophication turning from a macrophyte to a phytoplankton dominated state. The key idea is that a small basin of attraction may be used as a measure of resilience. A highly resilient system will nearly always return to its original state, hence its basin of attraction must be very large. Conversely, a non-resilient or fragile system is easily pushed out of one basin of attraction into another one.

Recall that the two states in our system have very different dynamical properties: the low-production state with low top biomass production and high variability, compared to the high-production state with high top biomass production and low variability. From an ecosystem function perspective, low variability or high biomass in higher trophic levels are beneficial for e.g. fish yield. Therefore, it may be desirable to keep the system on the high-production state.

While biomass production of a community is known to be mostly positively correlated with its functional diversity, we also found the high-production state in the food chain. This corresponds to, e.g., modern agricultural systems, which typically consist of monocultures with a low functional diversity, but a high biomass production available for higher trophic levels. However, even though such monocultures may produce more biomass than some functionally highly diverse mixtures, they are very fragile against external disturbances. In this way, functional diversity is regarded as an insurance against external perturbations. We clearly observed such an effect in our system, for both pulse and press perturbations, as illustrated by Fig. 5. Since the basin of attraction of the high-production attractor increases in size with \( \Delta \), the system becomes less likely to be pushed out of the basin of attraction by a pulse perturbation. This trend is persistent when varying not only the Hill exponents, but also the dilution rate, and the nutrient inflow concentration (Appendix A, Fig. A3), and is thus not limited to a particular part of the model's parameter space. In addition, the boundary crisis causing the sudden disappearance of high-production attractor (Fig. 5, black dashed line) is only present for low values of \( \Delta \). Hence, functional diversity also protects the high-production state from suddenly disappearing under a press perturbation.

Typical for a boundary crisis, the high-production state undergoes when decreasing \( \Delta \), are the long transients that are still present near the crisis point (Appendix C, Fig. C4). In an ecological context this could be problematic as such a long transient implies there is no way to know exactly when the crisis point has been passed and the basin of attraction no longer exists, until the system eventually accelerates towards the only remaining attractor. Such regime shifts were empirically observed by a variety of ecosystem models in different contexts, such as woodlands threatened by fires turning into grasslands, and shallow lakes threatened by eutrophication turning from a macrophyte to a phytoplankton dominated state. The key idea is that a small perturbation near the bifurcation point may move the system to an alternative stable state, but once this has happened, a much larger perturbation is needed in order to return back to the original state. It has been argued that, under certain circumstances, one may be able to observe early-warning signals that a transition is imminent. For example, near some types of bifurcations a dampening of the speed-of-return after a pulse perturbations may be observed, called critical slowing down. In the case of a boundary crisis, showing the existence of any early-warning signals has proven to be difficult. However, even if their existence could be shown mathematically, they will almost certainly be very difficult or impossible to detect in a real-life setting, where the exact chaotic dynamics may be obscured by measurement noise. Our results reveal that maintaining sufficient trait variation provides protection from boundary crises, with their often ecologically and economically undesirable consequences.

These conclusions rely on the presence of alternative stable states in our model. This is a prominent property in tritrophic systems, present in even a simple tritrophic chain with Holling-type-II functional responses and logistic growth of the basal species. However, there always exist parameter regions where there is only one non-trivial stable state. We find that also in such cases, production at the top level and temporal stability both increase with \( \Delta \), as the attractor changes from resembling the low-production to resembling the high-production state in a gradual way (See Appendix A, Fig. A6).
**Influence of a sigmoidal functional response.** The use of sigmoidal functional responses such as the (generalized) Holling type-III \((h = \eta > 1)\) has been an active area of discussion for quite some time. Sigmoidal functional responses are praised for their favorable effects on food web dynamics such as an increased dynamical stability\(^{36,81}\). Such an increase is justified by the apparent discrepancy between the observed stability of natural ecosystems, and the highly unstable nature of ecosystem models describing them\(^{35}\). While experimental evidence has traditionally mainly supported hyperbolic functional response shapes, such as Holling type-II \((h = \eta = 1)\)\(^{39,84}\), sigmoidal functional responses such as Holling-type-III provide models with additional stability which may overcome this discrepancy. Recent experiments studies have found evidence for sigmoidal functional response shapes\(^{37,85,86}\), or otherwise have shown the difficulty in distinguishing Holling type-II from type-III functional response shapes\(^{87}\). Furthermore, sigmoidal shapes account for natural processes not captured by the model such as spatial heterogeneity, refuges, formation of resting shapes, etc. Hence, Hill exponents close to—but higher than—one are likely to be relevant, and thus, the requirement of at least some grazing suppression at low densities for all species to coexist adds to the realism of the model. Even in the highly-controlled environment of the chemostat, some of the proposed mechanisms giving rise to the predation dampening at low prey densities, such as prey clumping\(^{88}\) or other induced defenses\(^{89}\), may well be of importance. In addition, while a Hill exponent larger than 1 does facilitate coexistence, it is not guaranteed. For example, Fig. 6c shows that one of the top predators is not able to survive for \(0 \leq \Delta \leq 0.1\).

Nonetheless, Fig. 5 also shows a significant, decreasing dependence on low prey density grazing suppression in order to reach the high-production state. For most of the range of \(\Delta\), the sharp border between the bistable region and the region where only the high-production state exists occurs at a lower value of the Hill-exponent as \(\Delta\) is increased. Hence, while the grazing suppression at low prey densities is necessary to reach the high-production state, it becomes a less important factor as \(\Delta\) is increased.

**Concluding remarks.** Despite the higher dynamical complexity of the resulting food web, the introduction of trait variation at all trophic levels to a linear food chain increased the overall reliability of ecosystem functions, such as resource use efficiency and high biomass production. Our results highlight that functional diversity on different trophic levels can reduce the overall temporal variability at the community level through compensatory dynamics among functionally different species within a trophic level. Investigating the phase relationships between the different species of adjacent trophic levels enabled us to identify the regulation of trophic interactions, such as changes in top-down or bottom-up control, in oscillatory dynamical regimes. Accordingly, we observed that strong deviations from the expected \(\frac{1}{3}\)-lag between predator and prey are possible in a tritrophic system, even without any trait variation. Hence, observation of such deviations do not necessarily indicate the presence of eco-evolutionary dynamics as is often assumed. Furthermore, independent of the presence or absence of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation, our tritrophic model shows two alternative states with the top predator exhibiting either a relatively low or high biomass. However, while the high-production state is attainable in a tritrophic food chain, its basin of attraction is very small. It becomes more resilient when trait variation is added, underlining the role of trait variation.
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