A Reliability-Aware Joint Design Method of Application Mapping and Wavelength Assignment for WDM-Based Silicon Photonic Interconnects on Chip

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ABSTRACT
Silicon photonic interconnects on chip is an emerging technology for future ultra-scale and data-intensive computing chips, e.g., many-core processors, owing to its high transmission speed and low latency. However, in the Wavelength Division Multiplexing (WDM)-based architecture, the communication reliability can be significantly affected by the signal losses and crosstalk, due to the inherent characteristic of photonic devices. This paper studies the influence on reliability of managing application mapping and wavelength assignment separately. To deal with this issue, we propose a reliability-aware joint design method coordinating application mapping and wavelength assignment schemes. For a given application core graph and a network architecture, the design method can obtain a result of application mapping and wavelength assignment with improved reliability, compared to the separate scheme. According to the evaluation of Optical Signal-to-Noise Ratio (OSNR), the proposed method enables more reliable communication under given applications.

INDEX TERMS
Silicon photonic interconnects on chip, design method, reliability, application mapping, wavelength assignment.

I. INTRODUCTION
Silicon photonic interconnects on chip is promising to improve the communication performance of the future multi-/many-core processors, providing high transmission speed and low latency for high-performance computing applications [1]. The development of silicon photonics makes it possible to integrate the required photonic devices, such as lasers, modulators, waveguides, and photodetectors, onto one single chip [2], [3]. At the same time, CMOS-compatible fabrication process allows photonic devices to be integrated with electrical interconnects, which is fundamental for future mass production.

In silicon photonic interconnects on chip, data is transmitted in optical waveguides in the form of optical signals. With WDM technology, multiple optical signals at different wavelengths can be delivered at the same time in one optical waveguide. This technology mainly relies on Microring Resonators (MRs) at different resonant wavelengths, which are utilized for modulating, routing, and filtering the optical signals based on the resonant wavelengths and signal wavelengths [4]. Compared to the manner of single-wavelength communication, the WDM-based communication can improve the communication bandwidth by $N_{WL}$ times [5], with $N_{WL}$ available wavelengths.
The communication reliability in WDM-based architectures can be affected by different aspects, such as the wavelength assignments for the specific communications. For instance, the communication reliability under the source-based wavelength assignment would vary [11] for the application mapping result shown in Figure 1.

However, the result of application mapping is based on a given wavelength assignment, while the result of wavelength assignment depends on a given application mapping result. If the application mapping or the wavelength assignment is managed separately, high signal loss and high crosstalk would be resulted into. Thus, in this work, we propose a reliability-aware joint design method of application mapping and wavelength assignment for the WDM-based silicon photonic interconnects on chip, based on reliability analysis model. The main contribution of this work is summarized as follows.

- A joint design method is proposed by taking into consideration of both application mapping and wavelength assignment, to reduce the signal loss and crosstalk, thereby improving the communication reliability. The correlation of application mapping and wavelength assignment is studied for the first time, to our knowledge.
- A reliability-aware application mapping scheme and a reliability-aware wavelength assignment scheme are designed, based on our reliability model. In this model, the transmission property of MR is used for the loss and crosstalk evaluation.
- The method is designed to be adaptable for different topologies and applications, with the flexibility of employing different optimization algorithms. In this work, ant colony optimization algorithm (ACO) is used for the illustration.

The rest of this paper is structured as follows. Section II presents the related work. Then, the network architecture and the reliability problem are described in Section III. Section IV presents the proposed reliability-aware joint design method. Section V details the proposed application mapping scheme and Section VI shows the wavelength assignment scheme. Section VII presents the OSNR model and Section VIII gives the case study and evaluation results. Section IX concludes the paper.

II. RELATED WORK

In this paper, the research on crosstalk-induced reliability issue is carried out in the WDM-based silicon photonic interconnects on chip, especially in the aspects of problem formation and solution.

In the WDM-based silicon photonic interconnects on chip, the communications in parallel between different pairs of source and destination nodes are specified by different resonant wavelengths. To utilize more wavelengths in optical communications can provide higher bandwidth. However, the coupling of optical signal at the MRs is not perfect. When the parallel communications at different wavelengths have some overlap with each other along the whole paths, the received signals at the destination side not only experience the optical losses unavoidably induced by the optical devices, but also can be affected by the crosstalk from other optical signals at different wavelengths. As a result, the OSNR of the expected signal would decrease, and thus the communication reliability would get worse, especially when many wavelengths are used for communication. In the worst case, the received signal might not be good enough for the correct communication [6], which leads to more laser power consumption [7], [8] for re-transmitting or more cost for signal correction. In the meantime, the scalability of photonic interconnect architecture is limited under a given laser power budget. Thus, to improve the OSNR is in turn possible to improve the power efficiency and the scalability.

Application mapping and wavelength assignment are two crucial aspects needed to be concerned. Firstly, the mapping result of a specific application can affect the relative locations of parallel communications in a network architecture, which thus influences the losses and crosstalk to an expected signal. Improper application mapping has a negative influence on the communication performance and reliability, which in return increases the laser power consumption [9]. For instance, an improper mapping result with the destination-based wavelength assignment is shown as the example in Figure 1. The communication \( c_6 \rightarrow c_7 \) experiences long routing path, leading to large signal losses. The communication \( c_4 \rightarrow c_7 \) has overlap with two other communications (i.e., \( c_6 \rightarrow c_7 \) and \( c_4 \rightarrow c_5 \)), resulting in large crosstalk for itself. Secondly, the wavelength assignment scheme can influence the crosstalk. For instance, if two adjacent wavelengths are assigned along one same optical path, the crosstalk can be greatly increased due to inevitable inter-coupling. In addition, different wavelength channel spacing can lead to different influences on the reliability [10]. So, different wavelength assignments for the specific communications, especially for the parallel ones, have different influences on the communication reliability in WDM-based architectures. For instance, the communication reliability under the source-based wavelength assignment would vary [11] for the application mapping result in Figure 1.
In the aspect of **problem formulation**, the existing research mainly focuses on the crosstalk model of WDM-based silicon photonic interconnects [12]–[17]. For instance, the OSNR of a ring-based Optical Networks-on-Chip (ONoC) and the crosstalk of a WDM-based ONoC are studied in [12] and [13] respectively, by considering fixed loss values of photonic devices from the state-of-art work as in [17]. These models can show a quantitative connection among the communication reliability, the crosstalk, and the scalability (detailed in Table 1 including ONoCs by using both single wavelength and multiple wavelengths). However, the influences of application property and wavelength assignment are not concerned.

In the aspect of **solution to mitigate the influence**, existing research mainly focuses on the architecture design [18], the system-level management schemes (e.g., DVFS, workload monitoring) [19], application mapping [20], [21], adaptive laser power control [22], redundant MRs and encoding [23], multilevel signaling [24], increase of wavelength spacing [25], wavelength allocation [9], etc. For instance, in [20], [21], an application mapping scheme is employed to reduce the worst-case crosstalk in the manner of reducing the number of communications in one waveguide, based on the pre-defined communication pattern of specific application. However, fixed loss values of photonic devices are considered in the work, and the influence of wavelength assignment is not considered, which would increase the crosstalk. In [22], an adaptive power control technique is used for the inter/intra-chip network to enhance OSNR. It can improve the laser power efficiency by allocating appropriate power strength when the communication pattern and routing path are both determined. In [23], double MRs and data encoding are employed to reduce crosstalk. In [24], four-amplitude-level optical signals are used to improve the reliability and energy efficiency. In [25], the OSNR is improved by reducing the number of multiplexed wavelengths, indicating that the increase of wavelength spacing between two adjacent wavelengths can lead to the reduced crosstalk. Besides, other approaches such as stochastic communication (or probabilistic flooding protocols), network coding, and reconfiguration in electrical NoCs [26]–[28] can be considered for the solution reference.

However, wavelength assignment is not taken into account in the existing schemes, i.e., power control and increase of wavelength spacing [22], [25]. A wavelength allocation scheme based on genetic algorithm is proposed in [9] to achieve a trade-off between performance and energy cost. This scheme mainly focuses on the optimization in the number of communication wavelengths, without the consideration of the wavelength spacing and the overlapping communications. Also, the communication case where each communication is performed on one wavelength is pointed out to be the most energy efficient [9]. In our work, the wavelength assignment scheme is designed under this case.

In addition, several static wavelength assignment schemes are proposed, e.g., source-based wavelength assignment [11], destination-based wavelength assignment [11], and communication-based wavelength assignment [29]. However, the influence of wavelength assignment on reliability is not considered.

In our proposed method, the application mapping and wavelength assignment are combined to improve the communication reliability at design time.

### III. RELIABILITY PROBLEM IN WDM-BASED SILICON PHOTONIC INTERCONNECTS ON CHIP

This section illustrates the reliability problem in WDM-based silicon photonic interconnects on chip based on the wavelength routing

Figure 2 illustrates a 3D network architecture to demonstrate the proposed method, as well as the case study. It is composed of i) an electrical layer implementing processing cores (in tiles) and memories, and ii) an optical layer with the implementation of CHAMELEON [30]. The activities of processing cores lead to both local and global communications which are realized by electrical interconnects in the electrical layer and photonic interconnects in the optical layer, respectively. The communication hierarchy is defined at design time, and depends mainly on the total number of processing cores and the complexity and bandwidth of photonic interconnects. Note that the proposed method is applicable for other

| Type of ONoC | Topology | Optical router | Network scale (OSNR, dB) |
|--------------|----------|---------------|-------------------------|
| ONoCs by using single wavelength | Mesh [14][15] | Optimized Crossbar | 6x6 (3.5dB) 16x16 (-13.9dB) |
| WDM-based ONoCs by using multiple wavelengths (e.g., 16 wavelengths) | Folded-Torus [15] | Optimized Crossbar | 14x14 (-1.8dB) 16x16 (-2.4dB) |
| Fat-Tree [16] | OTAR | 128 (-17.3dB) 128 (-17.3dB) |

*Figure 2. A 3D network architecture, implemented with CHAMELEON [30] at the optical layer, connecting IP cores at the electrical layer with TSVs.*
network architectures as well, while CHAMELEON is used for the demonstration of the proposed method.

The silicon photonic fabrication process is CMOS-compatible, and it allows integrating the required photonic devices, such as on-chip lasers, waveguides, MRs, and photodetectors. The silicon photonic devices (e.g., MRs) are mostly wavelength-selective, enabling the WDM technology and wavelength routing for high-bandwidth communication. These devices are assembled into so-called Optical Network Interfaces (ONIs), which are responsible for emitting the light, modulating optical signals with the data to be transmitted, and receiving them on the destination side (as shown in Figure 2). All the ONIs are connected via a ring bus waveguide propagating optical signals. Vertical-Cavity Surface-Emitting Lasers (VCSELs) and photodetectors are respectively connected to CMOS drivers and CMOS receivers through TSVs [6]. Multiple wavelengths are utilized at the optical layer for communications, enabled by MRs at different resonant wavelengths. CHAMELEON is implemented at the optical layer, and it is a ring-based network allowing reconfigurable communications between source and destination, with active MRs in ONIs. Also, it demonstrates less laser output power [30] compared to related optical crossbars including Snake [31] and SWMR (Single Write Multiple Read) modeled on ATAC [32].

Due to the configurability and regularity of the ONIs, different static wavelength assignment schemes can be used in the network, e.g., source-based wavelength assignment [11], destination-based wavelength assignment [11], and communication-based wavelength assignment [29]. The configuration of ONIs can be defined at either design-time or run-time.

However, different wavelengths can interfere with each other, due to the imperfect coupling in silicon photonic devices. Consequently, the OSNR of an expected signal is reduced after the transmission from the source to the destination, and the corresponding reliability is brought down. In the considered architecture, the laser output power is able to be controlled separately at local ONIs [30], according to the reliability requirement at the destination. This would contribute to the improvement of the laser power efficiency.

IV. RELIABILITY-AWARE JOINT DESIGN METHOD

In this section, we first analyze the influence on the communication reliability of managing application mapping and wavelength assignment separately. Then, an overview of the proposed reliability-aware method is presented. Afterwards, the application mapping and the wavelength assignment are introduced in detail.

A. INFLUENCE ON THE RELIABILITY OF MANAGING APPLICATION MAPPING AND WAVELENGTH ASSIGNMENT SEPARATELY

The result of application mapping has an influence on the received signal power and crosstalk at the studied node, thus resulting in an impact on the communication reliability. The locations of communications in a many-core processor are determined by the result of application mapping. It indicates different lengths of the routing path in one communication and different relative positions of all the communications. Meanwhile, the crosstalk is related to the routing paths of communications and wavelengths assigned to the communications [33].

For instance, the application core graph (in Figure 3-a) with four task cores includes two communications, i.e., $c_1 \rightarrow c_3$ and $c_2 \rightarrow c_4$. One example of application mapped to a network architecture (with four ONIs in ring topology) is shown in Figure 3-b. The communications $c_1 \rightarrow c_3$ and $c_2 \rightarrow c_4$ are mapped onto ONI$_1$ → ONI$_3$ and ONI$_2$ → ONI$_4$ respectively, with the communication wavelengths $\lambda_1$ (in red) and $\lambda_2$ (in blue). Due to the unwanted coupling of wavelength $\lambda_2$ along their overlapping path, the crosstalk to the communication $c_1 \rightarrow c_3$ is induced by the communication $c_2 \rightarrow c_4$.

However, the crosstalk is likely to be avoided when the result of application mapping is different. For instance, if the communications $c_1 \rightarrow c_3$ and $c_2 \rightarrow c_4$ are respectively mapped to ONI$_1$ → ONI$_2$ and ONI$_3$ → ONI$_4$ (in Figure 3-c), with the same wavelength assignment as Figure 3-b. There is no overlapping path between these two communications, leading to no crosstalk and higher reliability for communication $c_1 \rightarrow c_3$. The “overlapping” here refers to the simultaneous overlap both in space and in time. For instance, two communication pairs communicate with each other at different wavelengths along the same waveguide at the same time. In this case, we consider the two communication pairs to be “overlapping”. Our work is based on the worst case, on the assumption that all communication pairs can be executed simultaneously. As for the “temporal” feature when applying our method, this is what we are to consider in the future work with the evaluation under run-time application.

In addition, the crosstalk is also possible to be reduced by applying different wavelength assignments. For instance,
the wavelength $\lambda_3$ (in green) is employed for the communication $c_2 \rightarrow c_4$ in Figure 3-d, under the same mapping result with Figure 3-b. The transmission at three wavelengths is shown in details in Figure 4. In two cases of Figure 3-b and Figure 3-d, both the signals at $\lambda_2$ and $\lambda_3$ would be partially coupled into the MR at $\lambda_1$ and induce the crosstalk to the target signal at $\lambda_1$. The distance between $\lambda_2$ (and $\lambda_3$) and $\lambda_1$ is denoted as $d_{12}$ (and $d_{13}$). The crosstalk increases as the wavelength distance decreases, that is, the crosstalk induced by $\lambda_2$ is bigger than $\lambda_3$. Thus, compared to the case in Figure 3-b, the crosstalk (to the same communication $c_1 \rightarrow c_3$) decreases since the coupling of the wavelength $\lambda_3$ is much less due to a bigger distance between $\lambda_1$ and $\lambda_3$ (as shown in Figure 4), compared to that of the wavelength $\lambda_2$. Moreover, the crosstalk is also related to the number of used wavelengths for a given FSR (free spectral range). That is, if there are more available wavelengths for a given FSR, the spacing between two adjacent wavelengths (e.g., $\lambda_{\text{spacing}}$) would be smaller. And in this case, the crosstalk induced by other wavelengths to a targeted signal would be higher since the wavelength distance is smaller. Thus, to design a suitable wavelength assignment scheme for the communication (based on an optimal mapping result) is able to further decrease the crosstalk, and thus improve the communication reliability.

Therefore, different results of application mapping and wavelength assignment have different influences on the communication reliability, of which the worst-case OSNR (i.e., $\text{OSNR}_{\text{WC}}$) is to be taken as the evaluation metric. Under a given network architecture and application graph, to obtain the optimal mapping result, the searching space of mapping solutions increases with order of magnitude as the network scale augments, especially when considering the wavelength assignment at the same time. When the number of network nodes is $N$, there are $N!$ possible mapping results. For instance, the searching space is as large as $12! \approx 4.79 \times 10^6$ for mapping only 12 task cores in one-to-one way. This mapping problem is already proven to NP-hard [20], [34]. To get the optimal result with the traversal search, it is time-consuming and resource-hungry. The intelligent heuristic algorithms are a type of random search method that simulates the evolution of natural organisms or social group behaviors. Through the methods based on intuitive or empirical construction, they can provide some higher quality solutions under the reasonable computing resource conditions (such as computing time and space). Therefore, it is very suitable to use intelligent heuristic algorithms to solve the complex problems such as application mapping or wavelength assignment. The ant colony optimization (ACO) algorithm [35], [36] is one of the widely used intelligent solving algorithms. We utilize this algorithm only as a demonstrative example of solving tools. Based on our proposed method, other optimization algorithms such as genetic algorithm (GA) can also be used for the problem solving. The differences mainly include the parameter design rules and the implementation time of the algorithm.

The number of available wavelengths also has a direct influence on the size of the solution space. The bigger the number of available wavelengths, the larger the problem scale is. With larger problem scale, the designed algorithm can still solve the problem, but the required time of the solving process may become long. In the meanwhile, the solution space of the problem increases factorially. For a larger solution space, the time required to search for a higher-quality solution would also increase. Compared to the precise and exhaustive search method, the heuristic algorithm is able to greatly reduce the consumption of computing resources and time. It is similar regarding the number of increasing mapping nodes. Thus, a reliability-aware joint method is proposed in our work, in order to deal with this NP-hard problem. The method is focused on the joint consideration of application mapping and wavelength assignment, since these two aspects are correlated with each other in the WDM-based silicon photonic interconnects on chip. We are aware that the temperature variation would lead to an influence on the reliability, which would be explored in the future work.

B. OVERVIEW OF THE PROPOSED RELIABILITY-AWARE JOINT METHOD

In the proposed joint method (as shown in Figure 5), two aspects, i.e., application mapping and wavelength assignment, are considered. The network architecture and
application core graph are taken as the inputs. As for the evaluation of communication reliability, the optimal OSNR\(_{\text{WC}}\) (i.e., OSNR\(_{\text{WC, optimal}}\)) of all the communications is chosen as the metric.

Given the input of the proposed reliability-aware method, a specific application is first mapped onto the network architecture by using our proposed application mapping scheme (i.e., Phase I). Based on the mapping result of Phase I, we propose a reliability-aware wavelength assignment scheme (i.e., Phase II), assigning wavelengths based on communication pairs. At the Phase I, there is a need of certain wavelength assignment before our proposed assignment scheme (i.e., Phase II). So, destination-based wavelength assignment is applied at Phase I, since it can contribute a better result at the stage of application mapping. At the Phase II, our wavelength assignment scheme is proposed and performed based on the application mapping result in Phase I.

Finally, the results of application mapping and wavelength assignment with the OSNR\(_{\text{WC}}\) are output under the constraint of the mapping correspondence. The design space can be explored as well. The proposed joint method of application mapping and wavelength assignment can be implemented based on various optimization algorithms, corresponding to their characteristics. One heuristic algorithm, i.e., Ant Colony Optimization (ACO) algorithm, is used for the illustration of the proposed method. The ACO algorithm obtains the optimal result through the accumulation and renewal of pheromone along the path after a limited number of iterations, in consideration of the feedback information [35], [36]. It has capability of distributive, parallel, and global convergence. In the process of applying this algorithm, only some characteristics of the specific problem are added to the algorithm’s parameter design, in order to make the search proceed in the direction of problem solving. For instance, we take account of the objective function value in the pheromone update process, so that the result with a better objective value can leave more pheromone. Through such iterative search, the result with a better objective value can be screened out. However, at the beginning of iterations, the accumulation of pheromone costs a long time due to the lack of information, which results in a slow solving speed.

The related definitions of input information are shown as follows:

**Definition 1 (Application Core Graph):** is defined as ACG(C, E), where each vertex \(c_i \in C\) represents a task core and each directional edge \(e_{ij} \in E\) represents the communication from task core \(c_i\) to task core \(c_j\). The total number of vertexes is assumed to be \(V\) in the application core graph, and \(i\) and \(j\) are in the range of \([1, V]\).

**Definition 2 (Architecture Graph):** is defined as AG(T, H), giving how \(N\) network nodes are connected with each other in the physical network layout. The elements \(t_i \in T\) and \(h_{ij} \in H\) (\(i \in [1, N]\), \(j \in [1, N]\)) represent the \(i\)th network node and the physical link connecting the network nodes \(t_i\) and \(t_j\), respectively.

**Definition 3 (Communication Weight Matrix):** is defined as \(W = (w_{ij})_{V \times V}\), where the element \(w_{ij}\) indicates the volume of communication from task core \(c_i\) to task core \(c_j\). Here, \(i\) and \(j\) are in the range of \([1, V]\), and \(c_i\) and \(c_j\) belong to \(C\) in a given application core graph ACG(C, E).

**Definition 4 (Application Mapping Matrix):** is defined as \(M = (m_{ij})_{N \times N}\), where the element \(m_{ij}\) indicates the mapping result of a given task core \(c_i \in C\) in ACG(C, E) onto a network node \(t_j \in T\) in AG(T, H). \(M\) is a permutation matrix, and the

![FIGURE 6. The main procedure of the proposed method, with Phase I (i.e., application mapping scheme) and Phase II (i.e., wavelength assignment scheme).](image-url)
value of $m_{ij}$ is 1 when task core $c_i$ is mapped to the network node $t_j$. Otherwise, $m_{ij}$ is 0.

Definition 5 (Architecture Communication Matrix): is defined as $A = (a_{ij})_{N \times N}$, where the element $a_{ij}$ represents the communication weight of the network nodes $t_i$ to $t_j$ in the architecture after application mapping is applied. It can be obtained based on Communication Weight Matrix $W$ and Application Mapping Matrix $M$, as shown in equation (1).

$$A = M^T \cdot W \cdot M$$  

The mapping correspondence (in Figure 5), i.e., the rule of application mapping, is set as follows: i) each task core can be mapped to a network node; ii) two task cores are avoided to be mapped to the same network node. This correspondence is represented by equations (2), (3), (4), and (5).

$$\forall t, \sum_{t' \in T} \sum_{c' \in C, c' \neq c} a_{c't'} = 0$$  

$$\forall c, \sum_{t \in T} \sum_{c \in C} a_{ct} = 1$$  

$$\sum_{c \in C} \sum_{t \in T} a_{ct} \geq 0$$  

$$\sum_{c \in C} \sum_{t \in T} a_{ct} - V = 0$$  

In the proposed method, OSNRWC after mapping is set to be the optimization objective, defined as equation (6). That is, a minimum OSNR exists for the communications in $A$ after each iteration, and the objective is to maximize this minimum OSNR.

$$OSNR_{optimal} = \max \{\min(\{OSNR(A)\})\}$$  

B. SCHEME BASED ON ANT COLONY OPTIMIZATION (ACO) ALGORITHM

The application mapping scheme can be implemented with different optimization algorithms. In this section, the mapping scheme based on ACO algorithm is illustrated. $M$ ants are used to select all the task cores in the application core graph to the nodes in the network architecture during each iteration. After one iteration, only the ant which finds an optimal solution is to leave pheromone along the path being searched, to inspire the next iteration of the searching. Then the pheromone is updated before the next iteration. The placement of task core to network node is defined as a path between the ant colony and a food source. The path is evaluated according to the metric of the corresponding OSNRWC after application mapping. The max-min ACO algorithm [34] is adopted to avoid collapsing into a local optimal solution, which is caused by excessive accumulation or missing of pheromones. The detailed process is shown as the pseudo code of Algorithm 1 (in Figure 7), with the parameters defined in Table 2.

Each ant is characterized as follows: i) it executes a task independently, and only the ant which finds an optimal value of the objective leaves a pheromone along the path after each iteration; ii) the probability (i.e., $p$) of an ant to choose a network node for placing an task core depends on the pheromone along the path (i.e., $\tau$) and the heuristic information of the node (i.e., $\eta$); iii) ants follow the mapping rule that only one task core can be placed onto a network node, and this restriction is ensured with a tabu list in the algorithm. The related parameters are defined and updated as follows, under the given ACG(C, E) and AG(T, H).

1) ANT COLONY INITIALIZATION

In the first iteration, the ant colony is initialized, and there is no inspiration pheromone along the paths. The pheromone is initialized as $\tau_0$ along each path, and the selection probability of each task core is set to be the same.

2) CALCULATION OF SELECTION PROBABILITY

In the process of finding a solution, ants select the network node to place the task core through a random mechanism. For

Algorithm 1: Application mapping scheme based on ACO

| Parameter | Definition |
|-----------|------------|
| $M$       | The number of ants |
| $V$       | The number of task cores in the ACG(C, E) |
| $N$       | The number of network nodes |
| $OSNR_{optimal}$ | The worst-case OSNR corresponding to the optimal solution in the mapping scheme |
| $\tau_0$  | Initialized pheromone |
| $\alpha$  | Heuristic factor of information ($\alpha \in [1, 2]$) |
| $\beta$   | Expected heuristic factor ($\beta \in [2, 6]$) |
| $\rho$    | Evaporation coefficient of information ($\rho \in [0, 1]$) |
| $\eta_0(n)$ | Pheromone when mapping $c_i$ to $t_j$ at the $n$th iteration |
| $\Delta \eta^{max}$ | Pheromone increment that the ant with $OSNR_{optimal}$ leaves |
| $\rho_0(n)$ | Heuristic information when mapping $c_i$ to $t_j$ at the $n$th iteration |
| $K$       | A positive constant different from $Q(K\rightarrow OSNR)$ |

FIGURE 7. Pseudo-code of application mapping scheme based on ACO.
the ant \( m \) (\( m \in [1, M] \)) at the \( n \)th iteration, the probability of placing the task core \( c_i \) to the network node \( t_j \) can be calculated as follows:

\[
p_{ij}^m(n) = \begin{cases} 
\frac{[\tau_{ij}(n)]^\alpha [\eta_{ij}(n)]^\beta}{\sum_{t_k \in T^{m}_{\text{available},j}(n)} [\tau_{ik}(n)]^\alpha [\eta_{ik}(n)]^\beta}, & t_j \in T^{m}_{\text{available},j}(n) \\
0, & \text{else}
\end{cases}
\] (7)

Here, parameters \( \alpha \) and \( \beta \) determine the relative importance of the pheromone \( \tau_{ij}(n) \) versus the heuristic information \( \eta_{ij}(n) \). The selected nodes belong to the set \( T^{m}_{\text{available},j}(n) \), calculated by the following equation.

\[
T^{m}_{\text{available},j}(n) = T - T^{m}_{\text{used},j}(n),
\] (8)

where \( T^{m}_{\text{used},j}(n) \) represents the set of the already mapped nodes for the previous cores (i.e., \( c_1, c_2, \ldots, c_{i-1} \)) with the ant \( m \) at the \( n \)th iteration, and it is empty when \( i \) equals to 1. Based on the selection probability in equation (7), the bigger the pheromone (i.e., \( \tau_{ij}(n) \)) and the heuristic information (i.e., \( \eta_{ij}(n) \)) are, the higher the probability of placing task core \( c_i \) to network node \( t_j \) is.

According to communication characteristics of a specific application, the heuristic information \( \eta_{ij}(n) \) of mapping the task core \( c_i \) to the network node \( t_j \) can be defined as:

\[
\eta_{ij}(n) = \sum_{t_k \in T^{m}_{\text{used},j}(n)} \sum_{t_l \in T^{m}_{\text{available},j}(n)} d(j,k)
\] (9)

Here, \( d(j,k) \) is determined by whether there is communication requirement between node \( t_j \) (mapped by the core \( c_i \)) and the previously placed node \( t_k \) (mapped by the core \( c_i \in \{c_1,c_2,\ldots,c_{i-1}\} \)), indicating the correlation of two nodes. Its value can be calculated as follows:

\[
d(j,k) = \begin{cases} 
1, & \text{w/o communication between } t_j \text{ and } t_k \\
1+d_{jk}, & \text{w/ communication between } t_j \text{ and } t_k
\end{cases}
\] (10)

And \( d_{jk} \) is detailed as:

\[
d_{jk} = \begin{cases} 
|j-k|, & \text{or communication } t_j \rightarrow t_k \text{ exists} \& j < k \\
N-|j-k|, & \text{or communication } t_j \leftarrow t_k \text{ exists} \& j > k
\end{cases}
\] (11)

3) UPDATE OF PHEROMONE
To enhance the characteristic of superior solutions, the pheromone along the path is updated after each iteration, by increasing and decreasing the pheromone of superior and inferior solutions, respectively. The pheromone \( \tau_{ij}(n) \) is updated according to the following rules:

\[
\tau_{ij}(n+1) = (1-\rho) \cdot \tau_{ij}(n) + \Delta \tau_{ij}^{\text{max}}(n)
\] (12)

\[
\Delta \tau_{ij}^{\text{max}}(n) = \begin{cases} 
\frac{Q}{K - \text{OSNR}_{WC}} & \text{if core } c_i \text{ is mapped to node } t_j \\
0 & \text{otherwise}
\end{cases}
\] (13)

However, if the pheromone \( \tau_{ij}(n+1) \) is smaller than the lower limit \( \tau_{\text{min}} \) or bigger than the upper limit \( \tau_{\text{max}} \), it is set to be the corresponding boundary value, i.e., \( \tau_{\text{min}} \) or \( \tau_{\text{max}} \).

VI. RELIABILITY-AWARE WAVELENGTH ASSIGNMENT SCHEME
After obtaining the result of application mapping, a reliability-aware wavelength assignment scheme is proposed, employing the optimization algorithm, to further reduce the influence of crosstalk on the communication reliability. By taking into consideration of the distance of wavelengths assigned for the overlapping communications, the proposed wavelength assignment scheme can reduce the unwanted coupling in comparison with the traditional (static) schemes, e.g., source-based, destination-based, and communication-based wavelength assignment schemes. In this section, the proposed wavelength assignment scheme is first introduced, then the traditional wavelength assignment schemes are studied in detail.

A. THE PROPOSED SCHEME
In the proposed wavelength assignment scheme, the heuristic algorithms are applied to assign proper wavelengths for the communication paths, especially for the ones with overlapping. For the assignment, the “overlapping” in both space and time are considered simultaneously. Different communications can happen at the same time with the same wavelength if there is no spatial or temporal overlap between or among certain communications. Our work is based on the worst case, on the assumption that all communication pairs can be executed simultaneously. As a result, the proposed wavelength assignment scheme can minimize both the crosstalk suffered by the studied communication path and the crosstalk induced by the studied communication path to other paths. The main procedure of the proposed reliability-aware wavelength assignment is shown in the Phase II of Figure 6, of which the pseudo code is illustrated in Figure 8.

Based on the architecture communication matrix \( A \), communication information, e.g., the lengths and overlapping relationship of communication paths, can be obtained. The communication paths are firstly ranked according to their lengths, e.g., from the longest to the shortest, and stored in the path set \( \text{Path} = \{\text{path}_1, \text{path}_2, \ldots, \text{path}_j, \ldots, \text{path}_{n_{\text{path}}}\} \). The wavelengths that are available for communication are marked as a set \( \text{WL}_{\text{available}} = \{\lambda_1, \lambda_2, \ldots, \lambda_i, \ldots, \lambda_{N_{\text{WL}}}\} \), where \( N_{\text{WL}} \) indicates the total number of available wavelengths. Given the available wavelength range \( \text{WL}_{\text{range}} \), the wavelength \( \lambda_i \) is obtained by \( \lambda_i = \lambda_1 + \lambda_{\text{spacing}} \times (i-1) \), where the wavelength spacing \( \lambda_{\text{spacing}} \) can be calculated by \( \text{WL}_{\text{range}}/N_{\text{WL}} \). The wavelengths (in nm) in \( \text{WL}_{\text{available}} \) are assigned to communications by considering.


Algorithm 2: Wavelength Assignment scheme based on ACO

\textbf{Input:} architecture communication matrix \(A\)

\textbf{Output:} wavelength assignment result

\textbf{\textcolor{red}{Initialization}}\textcolor{black}{:}

Set parameters value \(M, \alpha, \beta, \rho, Q\)

Initialize all the pheromone values to \(r_e\)

\textbf{\textcolor{red}{\textcolor{red}{n}} Iteration}\textcolor{black}{:}

\textbf{for} ant \(m\) from 1 to \(M\) do

\textbf{for} \(i\) from 1 to \(N_{src}\) do

Generate a Tabu-search table \(Path_{tabu}(n)\)

Generate the allowed path set \(Path_{tabu}(n)\)

Calculate heuristic information according to adapted eq.(9)

\textbf{for} \(j\) from 1 to \(N_{dest}\) do

Calculate probability \(p_j^n(n)\) according to adapted eq.(7)

\(P_{\text{path}}(\text{sum}(p_j^n(n)), \text{where } k \in [1,j])\)

end for

\textbf{\textcolor{red}{\textcolor{red}{Roulette selection}}}:

Generate a random number \(NUM\), where \(NUM \in (0,1)\)

\textbf{if} \(NUM < P_j\) then

Select the \(path_j\) to assign the wavelength \(\lambda_i\), where \(path_j \in Path_{tabu}(n)\)

Move the assigned \(path_j\) to \(Path_{tabu}(n)\)

end if

end for

Calculate the objective value (i.e., \(OSNR_{WC}\)) for ant \(m\)

end for

Store the best wavelength assignment solution

Update pheromone information \(\tau(m)\) according to adapted eq.(12) for \(n\) iteration

\textbf{End Iteration}\textcolor{black}{:}

Return the best result after all the iteration, including the corresponding wavelength assignment result and \(OSNR_{WC}^{optimal}\)

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure8}
\caption{Pseudo-code of wavelength assignment scheme based on ACO.}
\end{figure}

\begin{table}[h]
\begin{tabular}{|c|c|c|c|c|c|}
\hline
\textbf{Symbol} & \textbf{Parameter} & \textbf{Value} \\
\hline
\(l_p\) & Propagation loss & -0.2744dB/cm \\
\(l_b\) & Bending loss & 0.005dB \\
\(\lambda_0\) & Initial wavelength of the considered range & 1550 nm \\
\(\text{FSR}\) & Free Spectrum Range, i.e., wavelength range & 59 nm \\
\(\Delta\lambda\) & Wavelength drift between ON and OFF states & 0.16nm \\
\hline
\end{tabular}
\caption{The parameters of the photonic interconnects on chip [33].}
\end{table}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9}
\caption{Source-based wavelength assignment scheme: a) the detailed rules; b) the assignment result of 4 network nodes.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure10}
\caption{Destination-based wavelength assignment scheme: a) the detailed rules; b) the assignment result of 4 network nodes.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure11}
\caption{Communication-based wavelength assignment scheme: a) the detailed rules; b) the assignment result of 4 network nodes.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure12}
\caption{Multiple-Write-Single-Read (MWSR); iii) communication-based wavelength assignment [29] (in Figure 11), in the manner of Multiple-Write-Multiple-Read (MWMR).

For the source-based wavelength assignment scheme, the communication wavelength \(\lambda_i\) used for any destination \(D_j\) (\(\forall j \in [1, N]\)) is assigned according to the ID of the source node \(S_i\). That is to say, the communications from the same source but to different destinations adopt the same wavelength \(\lambda_i\), depending on the source’s ID \(i\). For instance, the source node \(S_1\) transmits data to different destination nodes (e.g., \(D_1, D_2, D_3,\) and \(D_4\)) by using the same wavelength of \(\lambda_1\), as shown in Figure 9.

For the destination-based wavelength assignment scheme, the communication wavelength for any source node \(S_i\) (\(\forall i \in [1, N]\)) is assigned according to the ID of destination node \(D_j\). That is to say, the communications from different source nodes but to the same destination node adopt the same wavelength \(\lambda_j\), depending on the destination’s ID \(j\). For instance, the source node \(S_1\) transmits data to different destination nodes (e.g., \(D_1, D_2, D_3,\) and \(D_4\)) by using different wavelengths, i.e., \(\lambda_1, \lambda_2, \lambda_3,\) and \(\lambda_4\), as shown in Figure 10.

For the communication-based wavelength assignment, on one hand, the wavelengths can be assigned simply in a...}
regular way. For instance, Figure 11 demonstrates an example of communication-based wavelength assignment scheme with the Latin Square [38]. Similarly, the wavelengths can be assigned to communication paths in an ordinal order (i.e., C-based (O) for short), inverse order (i.e., C-based (I) for short), and random order (i.e., C-based (R) for short). For instance, communication paths are labelled as \{path1, path2, ..., pathN\}, which are extracted from the communication weight matrix \(W\). Then, the wavelength assignment result is \{\(\lambda_1, \lambda_2, ..., \lambda_N\}\} in the ordinal order, and \{\(\lambda_N, \lambda_{N-1}, ..., \lambda_1\}\} in the reverse order, corresponding to the IDs of communication paths. On the other hand, communication wavelengths can be assigned more flexibly. A reliability-aware scheme is used in this work, and the wavelengths are assigned according to the communication requirement and potential crosstalk, in order to reduce the influence of the crosstalk on the communication reliability.

VII. ANALYTICAL OSNR MODEL

This section presents the analytical OSNR model used in the proposed method to evaluate the communication reliability. Based on OSNR, BER (bit error rate) can be modeled and calculated [17]. The optical signal inevitably suffers insertion losses along the whole communication path from the source to the destination node, and experiences optical crosstalk from other different wavelengths at the same time if there are overlapping communications passing by the destination. The factors in network level determining the reliability are: network scale, network topology, the architecture of optical network interface, and the number of wavelengths.

A generic architecture with \(N_{ONI}\) interfaces is used as the illustrative example, and \(N_{WL}\) wavelengths are applied to emit and receive the optical signals, as shown in Figure 12. \(N_{WL}\) lasers and \(N_{WL}\) receivers, each at a specific wavelength, are employed to inject and eject optical signals in each interface respectively.

In the OSNR model, the optical signal at the wavelength \(\lambda_i\) transmitting from the source node ONI to the destination node ONI\(_d\) is analytically evaluated. The expected signal power at the destination node \(OP_{signal}\) is calculated as follows:

\[
OP_{signal} = OP_{in,i,j} \cdot L_{waveguide} \cdot \psi_{total,signal} \cdot \varphi_{signal}(\lambda_j, \lambda_i) \tag{14}
\]

where \(OP_{in,i,j}\) is the input signal power of ONI\(_i\) at the wavelength \(\lambda_i\). \(L_{waveguide}\) indicates the signal losses induced by the waveguide along the communication path, and it consists of the propagation loss and bending loss. \(\psi_{total,signal}\) represents the signal transmission efficiency at the through port of MRs along the communication path, and \(\varphi_{signal}(\lambda_j, \lambda_i)\) represents the signal transmission efficiency at the drop port of MRs in the source and destination nodes \([6], [33]\). \(\psi_{total,signal}\) can be calculated as follows:

\[
\psi_{total,signal} = \prod_{n=1}^{j-1} \varphi_l(\lambda_j, \lambda_n + d_n \cdot \Delta \lambda) + \prod_{n=1}^{N_{WL}} \varphi_l(\lambda_j, \lambda_n + d_n \cdot \Delta \lambda) \tag{15}
\]

where \(\varphi_l(\lambda_j, \lambda_n + \Delta \lambda)\) represents the signal transmission efficiency at the through port of MR, and \(\lambda_n\) is the resonant wavelength of the MRs encountered along the communication path. \(\Delta \lambda\) is the wavelength shift of an MR between its ON and OFF states. \(d_n\), of which the value can be 0 or 1, indicates the state of MR (i.e., ON or OFF) at the resonant wavelength \(\lambda_n\) along the communication path. In the network in Figure 12, when an MR is ON, it is used for detecting optical signal and drops the signal to the photodetector. Otherwise, the MR has no impact on the signal, and the signal passes by the MR and transmits along the waveguide. The parameter \(l_{s \rightarrow d}\) indicates the distance from the source to the destination of a studied communication. It can be calculated as follows:

\[
l_{ONI\rightarrow ONI_d} = \begin{cases} ONI_d - ONI_s, & \text{when } ONI_s < ONI_d \\ ONI_d - ONI_s + ONI_d, & \text{when } ONI_s > ONI_d \end{cases} \tag{16}
\]

For the expected signal at the wavelength \(\lambda_i\) in the destination interface ONI\(_d\), the crosstalk comes from the other signals at different wavelengths (emitted by the interface ONI\(_m\)) passing by the receiver in ONI\(_d\). For instance, the communication ONI\(_k\) \(\rightarrow\) ONI\(_{NONI}\) (at wavelength \(\lambda_i\)) in Figure 12 induces crosstalk to the expected signal of communication ONI\(_1\) \(\rightarrow\) ONI\(_i\) (at the wavelength \(\lambda_j\)) at the \(j^{th}\) receiver in ONI\(_i\). The crosstalk accumulated at the \(j^{th}\) receiver in the interface, i.e., \(OP_{crosstalk}[j]\), can be calculated as follows:

\[
OP_{crosstalk}[j] = \sum_{i \neq j} O_{crosstalk}[i][j] \tag{17}
\]

where \(O_{crosstalk}[i][j]\) indicates the crosstalk induced by the other signal at the wavelength \(\lambda_i\), and it can be calculated as follows:

\[
O_{crosstalk}[i][j] = O_{in,m,i} \cdot L_{waveguide} \cdot \varphi_d(\lambda_j, \lambda_i) \cdot \varphi_{total, crosstalk} \cdot \varphi_d(\lambda_i, \lambda_j) \tag{18}
\]

where \(O_{in,m,i}\) is the input power of ONI\(_m\) at the wavelength \(\lambda_i\). \(\varphi_{total, crosstalk}\) represents the crosstalk transmission efficiency at the through port of all MRs along the overlapping communication path. \(\varphi_d(\lambda_i, \lambda_j)\) represents the crosstalk transmission efficiency at the drop port of MR in the destination node. \(\varphi_{total, crosstalk}\) can be calculated as follows:

\[
\varphi_{total, crosstalk} = \prod_{n=1}^{N_{WL}} \varphi_l(\lambda_i, \lambda_n + d_n \cdot \Delta \lambda) \prod_{n=1}^{j-1} \varphi_l(\lambda_i, \lambda_n + d_n \cdot \Delta \lambda) \tag{19}
\]
On this basis, the OSNR model of optical communication from the source node ONI_s to the destination node ONI_d at the wavelength \( \lambda_j \) can be established as follows.

\[
OSNR_{s \rightarrow d}[j] = 10 \log \left( \frac{OP_{signal}[j]}{OP_{crosstalk}[j]} \right)
\]  

VIII. EVALUATION RESULTS

The case study for the proposed method is firstly detailed. Then the proposed method is validated and the performance improvement is studied. In the simulations, the proposed method is evaluated respectively under different applications and with different optimization algorithms. The influence of wavelength assignment schemes is analyzed afterwards, and the impact factors, i.e., wavelength spacing and wavelength drifts, are considered as well.

A. CASE STUDY

For the evaluation, a set of typical application benchmarks are considered, e.g., PIP, MWD, 263enc mp3dec, and mp3enc mp3dec [20], [39] respectively in Figure 13-a, -b, -c, and -d. These synthetic models of the real-world application benchmarks are also used in [20], [36], [40], [41], [42] to evaluate proposed strategies, different from the application modeling from high level programs to workload characterization for manycore platform design in [43]–[45]. The application benchmarks are abstracted into application core graphs (i.e., different directed graph), and the communications between various cores. The task core graphs in our evaluation are from [20], [39]. Each vertex in the application core graph represents a task core, and the directed edge represents the communication between cores. The communication volume exchanged between core are denoted by the weight of the edges. Note that the application benchmarks are utilized to evaluate the efficiency of the proposed method, but the method is not limited by the specific applications.

In our work, the network architecture in Figure 2 is used for application mapping, and it is able to assign wavelengths with the three different methods (i.e., source-based, destination-based, and communication-based wavelength assignments) by tuning on/off the corresponding MRs. The case studies are carried out on an Intel Core i5 platform with 3.0GHz clock frequency and 8GB memory space. The parameters related to photonic interconnects are from [33] and listed in Table 3. The number of wavelengths equal to the number of network nodes in the evaluation.

The application core graphs of different applications considered in the case study: a) PIP, b) MWD, c) 263enc mp3dec, and d) mp3enc mp3dec [20], [39].

FIGURE 12. Generic architecture for the establishment of the OSNR model.

FIGURE 13. Application core graphs of different applications considered in the case study: a) PIP, b) MWD, c) 263enc mp3dec, and d) mp3enc mp3dec [20], [39].
communication from core 1 to core 5, and the communication weight is 64MB/s [39].

For different applications, the communication weight matrix $W$ can be obtained from the application core graph, in consideration of the communication volume between the source core (“S” for short) and destination core (“D” for short). For instance, Table 4 gives the weight matrix of the application PIP, where “0” represents no communication exists, and the numbers indicate the volume of the related communications.

The application mapping matrix $M$ is obtained after mapping the application core graph to the network architecture (e.g., in Figure 1). One-to-one mapping is considered in the case study. The wavelength-routing communication is based on different wavelengths. In embedded systems, the process and interdependencies of application tasks in the real world are represented by means of application core graphs [39], and then the task cores are allocated to the available Processing Elements (PEs). In general, we execute the application mapping scheme as long as the number of task cores in the core graph is smaller than or equal to the network size. The resource is utilized more sufficiently when the number of task cores is equal to the number of network nodes, without idle network nodes. If the number of task cores is bigger than the number of network nodes, the task graph needs to be further divided before application mapping. That is to say, multiple tasks need to be allocated to a PE through scheduling process [46]. Different scheduling algorithms have been researched [46]. If the number of task cores is equal to or smaller than the number of network nodes, the application mapping can be performed directly.

In the application mapping matrix of Table 5, “1” represents that the corresponding task core is mapped onto the dedicated ONI, and vice versa for “0”. For instance, “1” is for task core 2→ONI 6 in the matrix, which represents that task core 2 is mapped onto the ONI 6.

The parameters used in the ACO algorithm is shown in Table 6-a. In addition, Genetic algorithm (i.e., GA) [47] is employed for the evaluation, to further show the flexibility of applying other optimization algorithms. GA is usually used to solve the unconstrained and constrained nonlinear optimization problems based on the natural selection process, mimicking the biological evolution. GA iteratively modifies the population consisting of individual solutions. In each step, GA randomly selects individuals from the current population and uses them as a parent to generate the next generation of children. After several generations, the group gradually “evolves” into an optimal solution. The related parameters are in Table 6-b.

### B. VALIDATION AND PERFORMANCE OF THE PROPOSED METHOD BASED ON ACO

In this subsection, the simulation results are first validated under the destination-based wavelength assignment, with the traversal mapping and random mapping schemes [36], [48]. In the traversal mapping, OSNR$_{\text{WC}}$ is evaluated for each mapping solution, namely 8! = 40320 mapping solutions are considered. In the random mapping, a given number of solutions are selected randomly.

Figure 14 shows the evaluation results of the OSNR$_{\text{WC}}$ under the application of PIP, with the traversal mapping (Figure 14-a and -b) and random mapping (Figure 14-c and -d). The distributions of OSNR$_{\text{WC}}$ with different mapping schemes are shown in scatter plots in Figure 14-a and -c. The probability distribution which highlights the statistical characteristics in scatter plots are shown in Figure 14-b and -d. According to the traversal mapping, the optimal OSNR$_{\text{WC}}$ is 47.1dB. Based on the scatter plots in Figure 14-a, most of the OSNR$_{\text{WC}}$ values are around 42dB with the highest probability, which accounts for about 90% of the results according to Figure 14-b.

From the results, the probability distribution of OSNR$_{\text{WC}}$ with random mapping shows a similar characteristic with the traversal mapping. For instance, OSNR$_{\text{WC}}$ in both mapping schemes reaches around 42dB with the highest probability,
according to Figure 14-b and -d. Compared to the traversal mapping, the optimal result with the random mapping can be obtained much faster, with 5000 mapping solutions instead of 40320. And the results with the random mapping are still representative by considering the distribution and statistical characteristic. Therefore, in this work the random mapping is used under the applications, since the traversal mapping requires more time and resources.

The proposed application mapping scheme is implemented based on ACO algorithm, to evaluate the OSNRWC under PIP. Figure 15 presents the results of our proposed method, with the related parameters set as Table 6-a. As the iteration number gets bigger, the OSNRWC increases gradually, and becomes stable at around 47.1dB finally, which equals to the optimal value obtained in traversal mapping in Figure 14.

Figure 16 illustrates the optimal OSNRWC and the consumed time (for obtaining the optimal OSNRWC) by utilizing different application mapping schemes, i.e., traversal mapping, random mapping, and the proposed mapping scheme based on ACO. The proposed mapping scheme can achieve a better tradeoff between reliability and time consumption, as shown in Figure 16. For the traversal mapping and the proposed method, their obtained optimal OSNRWC reaches 47.1dB, while it is 46.5dB for the random mapping. However, in the aspect of time consumption, the proposed method only costs 3.0s, while 16.2s and 1.8s for the traversal mapping and random mapping, respectively. To obtain the same OSNRWC, the proposed method takes about 81.6% less time than the traversal mapping. In the meanwhile, the search ability of our proposed scheme outperforms the random mapping due to the exploration of potentially optimal solutions.

C. ANALYSIS UNDER DIFFERENT APPLICATIONS BASED ON ACO

Figure 17 shows the evaluation results of random mapping under different applications, with 100,000 mapping solutions generated randomly. The scatter distribution and probability distribution are respectively given in Figure 17-a and -b. Most of the OSNR values fall in the range of 36dB to 38dB, and about 90% of the values are between 35dB and 40dB, below the biggest value of 42.8dB. Meanwhile, the random mapping takes ~111.5s to obtain the optimal results.

As shown in Figure 18-a, the proposed mapping scheme is evaluated with the same parameters as random mapping under the application of MWD [39]. As the iteration number progresses, the OSNRWC increases and finally reaches an optimal value, i.e., 44.6dB. Moreover, compared to the case in PIP, there are more task cores in MWD to be mapped, with more complicated communication characteristics, as shown in Figure 13. The optical signal might experience a longer communication path with more path overlapping, which induces less signal power and more crosstalk power. As a
result, the optimal OSNR$_{WC}$ under MWD decreases by 2.5dB compared to PIP. In addition, more times of iterations are required to reach the optimal value, due to the existence of more possible mapping solutions. For instance, the OSNR$_{WC}$ result gets stable at about 400 times of iterations under MWD, while at less than 100 times of iterations under PIP. To verify the accuracy of results, 200 rounds of simulations are performed with the same configuration, and it turns out that the optimal OSNR$_{WC}$ almost keeps the same with only ignorable fluctuation. Meanwhile, the proposed scheme takes about 48.4s in average for reaching the optimal value, which is about 50% less than the random mapping.

Similarly, the evaluation results under the applications of 263enc mp3dec and mp3enc mp3dec [39] are given in Figure 18-b and -c, respectively. In consideration of the communication patterns in Figure 13, similar conclusions can be achieved: i) the communication paths indicate less overlapping under 263enc mp3dec, thus the proposed mapping scheme can reach a higher OSNR$_{WC}$ of 47.3dB; ii) there are more task cores in the application core graph, and the communication paths are with more overlapping, thus the proposed mapping scheme gets a lower OSNR$_{WC}$ of 43.0dB.

D. ANALYSIS BASED ON DIFFERENT OPTIMIZATION ALGORITHMS

The proposed mapping scheme based on GA is evaluated under the applications of PIP, MWD, 263enc mp3dec and mp3enc mp3dec, and the corresponding results are shown in Figure 19-a, -b, -c, and -d, respectively. The OSNR$_{WC}$ reaches the optimal values of 47.1dB, 44.6dB, 47.3dB, and 43.0dB, respectively. The results are the same with the ACO algorithm. It can be observed that either ACO-based or GA-based scheme is able to perform a reliable search and obtain an optimal result, even if multiple run times are required.

E. ANALYSIS OF WAVELENGTH ASSIGNMENT SCHEMES

Wavelength assignment also has a significant influence on communication reliability. All the above evaluation results are obtained with the destination-based wavelength assignment. In Figure 20, OSNR$_{WC}$ of the three wavelength assignment methods (i.e., destination-based wavelength assignment, source-based wavelength assignment, and communication-based wavelength assignment) are explored under different applications.
The OSNR from task core 7 to task core 8 obtains the optimal OSNR $\text{WC} \rightarrow 8''$ of ''D-based'' indicates that the communication corresponding to the OSNR $\text{WC} \rightarrow i$ ferent communication pairs corresponding to the OSNR result in different mapping results, which may lead to dif-

The evaluation results of destination-based wavelength assignment exhibit the biggest OSNR$_{WC}$, e.g., 47.1dB under PIP, while the communication-based wavelength assignment with inverse order gets the smallest OSNR$_{WC}$, e.g., 45.4dB under PIP. This is because some communications sharing the same destination cannot communicate at the same time, resulting in less crosstalk. It is necessary to design a proper wavelength assignment scheme, to obtain a higher reliability and fulfill more communications at the same time. According to the results, the destination-based wavelength assignment always gets the highest OSNR$_{WC}$, and this is the reason why it is used in the previous analysis.

Meanwhile, different wavelength assignment schemes result in different mapping results, which may lead to different communication pairs corresponding to the OSNR$_{WC}$. As shown in Figure 20, “i $\rightarrow$ j” represents the task cores corresponding to the OSNR$_{WC}$ of each case. For instance, “7 $\rightarrow$ 8” of “D-based” indicates that the communication from task core 7 to task core 8 obtains the optimal OSNR$_{WC}$ under PIP with the destination-based wavelength assignment.

It can be observed that different wavelength assignment schemes correspond to different task cores with the OSNR$_{WC}$. That is because the optimal mapping results are different when the wavelength assignments are constrained. In addition, it illustrates that destination-based wavelength assignment contributes a better result of OSNR at this stage of application mapping under a same application. This is the reason why we utilize the destination-based wavelength assignment at Phase I of our proposed method.

The mapping results (in Figure 20) with different wavelength assignment schemes under PIP are given in Figure 21, together with the wavelength assignment results. For instance, the OSNR$_{WC}$ of “D-based” corresponds to the communication of task core 7 $\rightarrow$ 8, i.e., ONI 1 $\rightarrow$ 2 in the mapping result of Figure 21-a, with the assigned wavelength $\lambda_1$. The OSNR$_{WC}$ of “C-based (I)” corresponds to the communication of task core 1 $\rightarrow$ 2, i.e., ONI 2 $\rightarrow$ 3, with the assigned wavelength $\lambda_8$, as shown in Figure 21-d.

To further analyze the influence of wavelength assignment scheme, OSNR$_{WC}$ obtained by using the proposed mapping scheme is evaluated, along with other wavelength assignment schemes. The same application graph and same mapping result are considered, and the results of OSNR$_{WC}$ are shown in Figure 22. Under the same mapping result, the wavelength assignment by adopting the proposed method contributes the best OSNR$_{WC}$. For instance, “C-based (Proposed)” achieves an OSNR$_{WC}$ of 51.3dB, while “D-based” obtains 47.1dB under the same mapping result in Figure 21-a. Thus, the proposed wavelength assignment can achieve an improvement of 4.2dB at least, compared to the other wavelength assignment schemes.

It can be observed that the different wavelength assignment not only perform differently on reliability results, but also lead to different corresponding communications. For instance, the OSNR$_{WC}$ of “C-based (Proposed)” corresponds to the communication of task core 3 $\rightarrow$ 4, while the OSNR$_{WC}$ of “D-based” corresponds to task core 7 $\rightarrow$ 8 under the same mapping result in Figure 21-a. It is assumed that only one wavelength is assigned to a communication, without the consideration of the communication weight. However, the communication with higher weight can be assigned with more than one wavelength, to increase the throughput and reduce the communication delay. This would be explored as a part of the future work, by considering a compromise between the reliability and the communication delay. Our method is designed to reach the result with higher reliability and less time. The reduced time is due to the reduction of the search space brought by both the optimization algorithm and the problem decomposition.

F. EXPLORATION ON THE WAVELENGTH CHANNELS

As shown in Figure 23, the communication reliability of the proposed method is further explored under different
wavelength spacings (i.e., $\lambda_{\text{spacing}}$) between the adjacent wavelength channels, and under different wavelength drifts (i.e., $\Delta \lambda$) between the ON and OFF state of MR.

For the case of PIP mapped onto 8 ONIs, eight wavelengths are utilized for communication with the $\lambda_{\text{spacing}}$ of 8.43nm and $\Delta \lambda$ of 0.16nm [33]. The wavelength spacing will be smaller when more wavelength channels are used in the range of a given FSR, and the wavelength drifts will be different when the MRs are designed differently. The influence of these two factors on OSNR$_{\text{WC}}$ is investigated, ensuring the wavelength drift would not result in wavelength overlapping or disorder of wavelength channels. That is to say, the wavelength after drift from ON to OFF is still in the range of initial wavelength and the next wavelength channel. For instance, $\lambda_1 + \Delta \lambda$ is smaller than $\lambda_2$, as shown in Figure 4. In the evaluation results, OSNR$_{\text{WC}}$ gets smaller as $\lambda_{\text{spacing}}$ decreases under the same $\Delta \lambda$. This is induced by the increasing crosstalk under a constant signal power. At the same time, OSNR gets smaller as $\Delta \lambda$ increases under the same $\lambda_{\text{spacing}}$. This is because the optical signal power keeps almost the same level while the crosstalk increases due to the smaller spacing between two adjacent wavelengths.

In addition, under a given FSR, the total number of available wavelengths is limited, since the spacing between two adjacent wavelengths would decrease as the number of wavelengths increases. Thus, more wavelengths correspond to increasing crosstalk and decreasing communication reliability. With the continuous increase of the number of communication pairs, it is not sufficient to support all the parallel communication pairs with just the strategy of reusing wavelengths. Other strategies are necessary to be considered for supporting the communication. For instance, spatial multiplexing by adding more waveguides in a given architecture can be used (for example in MRONoC [11]), so that the limited number of available wavelengths are reused in different waveguides to improve the communication performance.

Therefore, the number of wavelengths used for communication needs to be properly studied for the tradeoff of performance and reliability.

**IX. CONCLUSION**

In this paper, we propose a novel joint method to map the applications onto the network architecture, with the consideration of wavelength assignment to improve communication reliability. Two aspects, i.e., application mapping and wavelength assignment, are considered in this work. Different optimization algorithms, e.g., ACO and genetic algorithms, are applied and evaluated in the proposed method. This method is universal to employ different optimization algorithms. In the evaluation of accuracy and efficiency, different applications are considered in implementing the mapping with the proposed method. The influence of different wavelength assignment schemes is evaluated, and a reliability-aware wavelength assignment scheme is proposed to use to improve the reliability jointly. The evaluation results indicate that the mapping considering the wavelength assignment can lead to better reliability. The design space, e.g., the influence of the wavelength spacing between two adjacent wavelengths and the wavelength drift between ON and OFF state, is further studied. This work is mainly focused on the proposed reliability-aware joint design method. In the future, the work will be done in the aspects of the exploration of other efficient optimization algorithms, the design of runtime mapping scheme, and the application mapping considering the thermal effect.
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