Low-frequency lattice phonons in halide perovskites explain high defect tolerance toward electron-hole recombination

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Low-cost solution-based synthesis of metal halide perovskites (MHPs) invariably introduces defects in the system, which could form Shockley-Read-Hall (SRH) electron-hole recombination centers detrimental to solar conversion efficiency. Here, we investigate the nonradiative recombination processes due to native point defects in methylammonium lead halide (MAPbI3) perovskites using ab initio nonadiabatic molecular dynamics within surface-hopping framework. Regardless of whether the defects introduce a shallow or deep band state, we find that charge recombination in MAPbI3 is not enhanced, contrary to predictions from SRH theory. We demonstrate that this strong tolerance against defects, and hence the breakdown of SRH, arises because the photogenerated carriers are only coupled with low-frequency phonons and electron and hole states overlap weakly. Both factors appreciably decrease the nonadiabatic coupling. We argue that the soft nature of the inorganic lattice with small bulk modulus is key for defect tolerance, and hence, the findings are general to other MHPs.

INTRODUCTION

The metal halide perovskites (MHPs) have enormous potential for optoelectronic applications including solar cells and light-emitting diodes. Several studies have shown that methylammonium lead halide perovskites MAPbX3 (MA = CH3NH3; X = Cl, Br, I), and especially MAPbI3, have many unique properties, such as high optical absorptions (1, 2), long electron-hole (e-h) diffusion lengths (3, 4), shallow dominant point defects (5–7), and electronically benign grain boundaries (7, 8). Because of intensive research and interest in these materials, we have witnessed, in the past 10 years, a marked increase in the power conversion efficiencies (PCEs) of MHP-based solar cells from 3.5 to 23.3% (9), which is comparable to record efficiencies of commercial thin-film copper indium gallium diselenide and CdTe-based solar cells (10, 11). Nevertheless, the reported PCE is still inferior to the Shockley-Queisser’s theoretical limit of 30 to 33% for solar absorbers with band gaps in the 1.2 to 1.6 eV energy range (12, 13). This calls for a better understanding of efficiency losses due to electron-hole recombinations that are predominantly nonradiative (14–16).

The low-cost synthesis of perovskites is one of the main attractive features of these new photo-absorbers. However, because of the relatively soft ionic nature of MHPs, this approach will invariably introduce different intrinsic or extrinsic dopants in the system (17–20). In traditional semiconductors, cation or anion doping can produce defect states in the band gap, which may form e-h recombination centers via the Shockley-Read-Hall (SRH) process, and consequently suppress the solar energy conversion efficiency by converting the photon energy into heat (21). While several theoretical studies concluded that thermodynamically stable intrinsic defects in MAPbI3 have relatively shallow defect states and hence are electronically benign (1, 6, 7, 22, 23), these conclusions are based on static T = 0 K calculations without accounting for the inelastic electron-phonon interactions. Given that the effective working temperature of a solar cell at room temperature with a PCE of 20% exceeds 343 K (24), temperature effects cannot be ignored. Previous studies have shown that temperature plays a notable effect on solar efficiency such as decreasing the open-circuit voltage Voc of MAPbI3-based solar cells from 1.01 to 0.83 V as the temperature increases from 300 to 360 K (25). In part, Voc drop could be due to the renormalization of the band gap of MAPbI3 with temperature, which is of the order of 30 to 40 meV in the temperature range of solar cell operation (26–29). In addition, the degradation of PCE with temperature could be due to enhancements in the inelastic scattering between defect and charged carriers, as these are mediated by electron-phonon coupling. Although a couple of studies have recently investigated nonradiative processes in MAPbI3 (30, 31), a comprehensive understanding of how defects affect the e-h recombination in the MHPs and how these differ from traditional semiconductors is still lacking.

Here, we study, in detail, the interplay between nonradiative e-h recombination processes and point defects in MAPbI3 using a nonadiabatic molecular dynamics (NAMD) approach. Considering only the intrinsic point defects in MAPbI3, there are three types of vacancy defects (Iv, PbV, and MAV), three interstitial defects (Ii, MAVi, and PbI), and six antisite defects (IiMA, MAV, PbI, IiPb, PbiMA, and MAPb, where Ab indicates that A is substituted by B). Among these 12 types, we focus our study on defects that have low energy formations and thus are abundant during synthesis. These include 1 interstitial (Ii), 1 MA substituted by I (MAi) or Pb (MAPb), Pb vacancy (PbV), and I vacancy (Ii) (7). While these defects are found to display distinctly different electronic structures by either having mid-gap or shallow p- or n-type defect states, we show that surprisingly these defects do not accelerate e-h recombination. We find that the charge recombination for the Ii...
system is even suppressed by a factor of 2 compared to the pristine system. We further find that for both the pristine and defective systems, the photogenerated carriers are only coupled with low-frequency phonons, which notably decrease the nonadiabatic coupling (NAC) between the donor and acceptor states. Therefore, both the pristine and defective systems have a long $e$-$h$ recombination time. We propose that these conclusions are general for all hybrid organic-inorganic perovskite solar cells and may extend to other semiconductors with low-frequency lattice phonons.

**RESULTS**

Before investigating the $e$-$h$ recombination dynamics, it is instructive to study the static (0 K) electronic structure of the different defective systems. The optimized atomic structure of the five defects and their corresponding density of states (DOS) are shown in Fig. 1. For comparison, we also show the results of the pristine system. One can see that $I_i$ and $Pb_V$ introduce shallow defect states near the valence band maximum (VBM), while $MA_{Pb}$ and $I_V$ introduce shallow defect states near the conduction band minimum (CBM). MA$_I$, on the other hand, introduces a deep defect state located 1.4 eV above the VBM. On the basis of the electronic structure, we can regard $I_i$ and $Pb_V$ as p-type defects as well as $I_V$ and $MA_{Pb}$ as n-type defects, whereas MA$_I$ can be considered as a neutral defect. The calculated electronic structures of these defects are consistent with our previous study using a larger supercell and spin-orbit coupling (SOC) correction (7). Further, we verified that the results are consistent with the Heyd-Scuseria-Ernzerhof (HSE06) + SOC electronic structure, except for $I_i$, in which we find the defect shallow state obtained with Perdew-Burke-Ernzerhof (PBE) to split into a shallow and deep state (fig. S3) (17). Nevertheless, as we discuss in the Supplementary Materials, this does not appreciably affect the recombination rates (section S2).

Electron-phonon interactions can have notable effects on the electronic structure of the system. Figure 2 shows the time evolution of the frontier and defect energy levels at 300 K. Only $I_i$ and $MA_{Pb}$ have shallow defect states close to the VBM and CBM, respectively (Fig. 2, A and C), while $MA_{I}$, $Pb_V$, and $I_V$ introduce defect states in the band gap (Fig. 2, B, D, and E). Further, as can be seen from the figure, the modulations of the defect states along the molecular dynamics (MD) trajectory are more notable compared to those of the VBM and CBMs. This is somewhat expected, given that the defect state is associated with a number of broken bonds that are less rigid during the MD (fig. S4).

Following a photoexcitation, the electron-phonon coupling can induce a direct nonradiative recombination of electrons and holes on CBM or VBM or via a by-defect nonradiative recombination mediated by the defect states, as is shown schematically in Fig. 3A. The direct path commences with an electron (hole) hopping to the VBM (CBM), followed by $e$-$h$ recombination. The by-defect path is more complex with different nonradiative carrier relaxation pathways. For example, a captured excited hole by the defect either can recombine with an electron in place after hopping to the conduction band or can even thermally escape and relax back to the VBM without any recombination if the energy barrier could be overcome by thermal fluctuations. Similar pathways exist for the electron, as shown in Fig. 3A. The overall nonradiative $e$-$h$ recombination that deteriorates the efficiency of the solar cell is the result of the competition between all of these processes, which are described using the NAMD framework. Radiative and Auger $e$-$h$ recombinations are not discussed in this work.

Figure 3B depicts the direct and by-defect recombination rates from the NAMD dynamics following a photoexcitation after evolving the system for 2 ns. Figure 3 (C and D) depicts the time changes of the direct and by-defect rates over 2 ns for the two pathways, which are used to estimate the $e$-$h$ lifetime. For the pristine system, Fig. 3B shows that ~19% of the different sampled $e$-$h$ trajectories terminate with a nonradiative recombination with an estimated $e$-$h$ lifetime of ~11 ns. Despite the distinct nature of the defect states, Fig. 3B shows that there is no notable acceleration of charge recombination in the...
defected systems in comparison to the pristine one, even after incorporating the new by-defect carrier pathways. The charge recombination rates are found to be ~17% (MA Pb ), 17% (MA I ), 24% (I V ), and 25% (MA I ), which are comparable with the rate obtained in the pristine system. In addition, the corresponding charge recombination rate time scales are similar to the pristine system. In contrast to the other defects, surprisingly, I V is found to notably suppress the recombination rate to ~9%, which is less than half the value of the pristine MAPbI 3 . This results in a longer e-h recombination lifetime of ~23 ns for I V . The slower charge recombination time reduces electronic energy dissipation into phonons and enhances photon-to-electron conversion efficiency.

The predicted NAMD nanosecond time scales of the e-h recombination are underestimated compared with the lifetime measured experimentally in neat MAPbI 3 (3, 4, 32). This is likely due to confinement effects introduced by the small unit cell, which limits the carriers’ diffusion and thus increases the probability of scattering and recombination. Given the computational cost of first-principles calculations, it is not practical to simulate realistic system size that would be of the order of 20 × 20 × 20 supercell with 40,000 atoms. To assess finite size effects, we used a larger 2 × 2 × 2 supercell with 384 atoms. Figure S1 shows that the e-h recombination time increases with systems size from 11 to 64 ns. Assuming that the e-h scattering probability is linearly proportional to the volume of the unit cell, we can estimate the lifetime of the 20 × 20 × 20 supercell to be of the order of 60 μs. Although this time scale is in line with recent experimental values, more investigations are needed to accurately determine the lifetime. Although issues related to finite size effects are shown in fig. S1, we show in the Supplementary Materials that the relative magnitude in the e-h recombination rates between the pristine and defective MAPbI 3 is less sensitive to the unit cell size (section S1).

As have been discussed in the previous studies (33, 34), the e-h recombination rate is strongly dependent on the NAC between the donor and acceptor states. The NAC matrix element djk can be expressed as

$$d_{jk} = \langle \phi_j | \frac{\partial}{\partial t} | \phi_k \rangle = \frac{\langle \phi_j | [\nabla_R H]_{\phi_k} \rangle}{\epsilon_k - \epsilon_j} R$$  

(1)

where $H$ is the Kohn-Sham (KS) Hamiltonian; $\phi_j, \phi_k, \epsilon_j,$ and $\epsilon_k$ are the wave functions and eigenvalues for donor and acceptor states $j$ and $k$, respectively; and $R$ is the nuclear velocity (34). The first equality in Eq. 1 shows that the NAC is due to the overlap between two orbitals at adjacent ionic time steps along the MD trajectory. The second equivalent representation of the NAC matrix in Eq. 1 shows more clearly that $d_{jk}$ depends on the energy difference $\epsilon_k - \epsilon_j$, the electron-phonon coupling term $\langle \phi_j | V_{e-p} H \phi_k \rangle$, and the nuclear velocity term $R$. In the e-h recombination NAMD dynamics, the donor and acceptor states include the CBM, the VBM, and the defect state. Because the NAC varies with atomic configurations, we report in Table 1 the root mean square NAC values between the different states to quantify the coupling strength along the MD trajectory. As we will argue next, the average NAC can provide a good understanding of the e-h dynamics reported in Fig. 3.

The NAC between CBM and VBM of the pristine system is 0.69 meV, which is larger than all corresponding values for the defective systems as shown in Table 1. This indicates that the recombination of free carriers in the CBM and VBM is suppressed in the defective systems. However, as shown in Fig. 3 (B and C), the probability for recombination via the direct path in the defected systems is markedly smaller than that of the pristine one. This apparent inconsistency is because the NAC between defect with either CBM or VBM is larger by one order of magnitude than that between CBM and VBM. Therefore, the electron or hole is likely to be trapped by the defect, and thus, the charge dynamics in these defective systems are mainly driven by the by-defect path and concurrently suppressing recombination via the direct path.

Further, examining the coupling values for the by-defect route in Table 1, we see that while for MA Pb, Pb V , and I V , the NAC matrix element between the CBM and the defect state is relatively large (10.25, 3.98, and 7.03 meV, respectively), the corresponding NAC values between the defect state and the VBM are notably smaller (0.56, 0.35, and 0.59 meV, respectively). These NAC values suggest that MA Pb, Pb V , and I V defects will capture an excited electron with a high probability but are less likely to trap a hole. Therefore, the e-h recombination due to the defect states will not be facile, with the hole capture being rate limiting. Similarly, the charge recombination for I V systems is also hindered because the defect has a weak coupling for the electron despite being a hole trap state. For the neutral MA I defect, the NAC matrix elements between the VBM and the defect state are 0.46 (1.25) meV, which are of similar magnitude. Therefore, the MA I system with the mid-gap state is a potential e-h recombination center. As shown in Fig. 3B, the by-defect charge recombination in MA I is the fastest among the five systems we have investigated. However, the recombination rate is not appreciably accelerated because of the small NAC values (0.46 meV). From this analysis, it can be seen that the by-defect e-h recombination is mostly determined by the smallest NAC among the VBM, the CBM, and the defect state. This is referred to as effective NAC. In summary, regardless of the defect type, the effective NAC for charge recombination in the defective MAPbI 3 systems is smaller than that of the pristine system.

The NACs between different states strongly depend on the phonon excitation and electron-phonon coupling, which can be understood from the fluctuations in the band energies shown in Fig. 2. The phonon excitations that coupled to the electron subsystem can be determined by examining the (normalized) autocorrelation function $C(t) = \langle E(t)E(0) \rangle / \langle E(0)E(0) \rangle$ for the state energy $E(t)$, where the
brackets (…) indicate canonical averaging. A rapid decay of $C(t)$ from 1 to 0 indicates that the fluctuations are driven by many vibrations, while a periodic oscillatory behavior indicates that few modes couple to the electron subsystem. Figure 4 shows the Fourier transform of $C(t)$ for the VBM, the CBM, and the defect state energies, which is generally used to analyze the phonon frequencies due to electron-phonon coupling (34). First, one can see that for all the different systems, the frequencies of the dominant phonon modes are below 100 cm$^{-1}$. The low-frequency phonon modes are associated with heavy mass atoms that have appreciably small nuclear velocities and consequently result in small NAC as seen from Eq. 1. These low-frequency phonon modes are the optical phonons contributed by the inorganic Pb-I lattice (35, 36). On the other hand, the absence of appreciable peaks in the 150 to 3500 cm$^{-1}$ range indicates that MA molecular vibrations are not coupled with the CBM, the VBM, or defect states. Note that our MD trajectory (~10 ps) is long enough to capture the rotational dynamics of MA that has a ~7 ps time scale at 300 K (37). Further, the negligible role of MA, if any, in influencing

| Table 1. The root mean square of NAC between the VBM, the CBM, and the defect states for different systems. |
|---|---|---|
| | NAC (meV) |  |
| | VBM-CBM | VBM-defect | CBM-defect |
| Pristine | 0.69 |  |
| $I_1$ | 0.56 | 7.17 | 0.58 |
| MA$_i$ | 0.55 | 0.46 | 1.25 |
| MA$_{pb}$ | 0.57 | 0.56 | 10.25 |
| Pb$_v$ | 0.63 | 0.35 | 3.98 |
| $I_v$ | 0.63 | 0.59 | 7.03 |

Fig. 4. The Fourier transform spectra of the autocorrelation function of the VBM, the CBM, and the defect state energies. (A to F) Defective and Pristine systems of MAPb$_3$.
the NAC is justified because MA does not contribute directly to the frontier orbitals (38) or even to the defect states (vide infra). In addition, this is consistent with conclusions drawn before using a similar NAMD approach (31).

Figure 5 shows the distribution of the electron density for the frontier and defect orbitals for a configuration extracted from the MD trajectory. For the pristine system, in agreement with previous investigations, the VBM and CBM are distributed mainly on I and Pb atoms, respectively (38). As seen from Fig. 5, the native defects in MAPbI₃ localize the CBM and VBM electron distribution due to strong distortions in the lattice. This localization, in turn, decreases the overlap between the orbitals at neighboring time steps, which explains the decrease in the NAC (see Table 1). The defect states are also localized as shown in Fig. 5, which also reduce the NAC, thus supporting the relatively small effective NAC values for KS orbitals that are not close in energy. In the case of Iᵢ, Fig. 5A shows that, near an iodine interstitial, the electron density is depleted for the VBM and CBM but enhanced for the defect state. This charge redistribution appreciably decreases the NAC, which thus suppresses the e-h recombination rate. During the MD, there can be strongly disordered structures, as have been discussed in previous investigations (39), which also reduce the NAC.

To explore the impact of SOC on our results, we have extracted on the order of 10 different configurations from the MD trajectory and computed the NAC using the adiabatic self-consistent spinor wave function, \( \psi(r,t) = (\phi_+(r,t), \phi_-(r,t)) \), where \( \phi_+ \) and \( \phi_- \) are the two spinor components. The configurations are selected such that their NAC matrix elements with PBE are similar to the average values shown in Table 1 to capture the most observed behavior. Using the spinor basis sets, we computed the NAC using the Hammes-Schiffer and Tully equation (40).

\[
d_{jk} = \left\langle \psi_j | \frac{\partial}{\partial t} | \psi_k \right\rangle \\
= \frac{1}{2d} \left\{ \langle \psi_j(r,t) | \psi_k(r,t+dt) \rangle - \langle \psi_j(r,t+dt) | \psi_k(r,t) \rangle \right\} \\
= \frac{1}{2d} \left\{ \langle \phi_{j+}(r,t) | \phi_{k+}(r,t+dt) \rangle + \langle \phi_{j-}(r,t) | \phi_{k-}(r,t+dt) \rangle - \langle \phi_{j+}(r,t+dt) | \phi_{k+}(r,t) \rangle - \langle \phi_{j-}(r,t+dt) | \phi_{k-}(r,t) \rangle \right\}
\]

As we show in Table S1, the NAC matrix elements with PBE + SOC are much larger than those obtained using PBE, which is understood because the band gap with PBE + SOC is notably underestimated compared to the PBE band gap, and the NAC is inversely proportional to eigenvalue differences as seen in Eq. 1. However, despite this, we can see that the relative values between the NAC PBE + SOC and PBE matrix elements are similar, suggesting that our findings will not be affected by ignoring SOC. For example, from the NAC values associated with the defect state, we conclude that MAₚb, Pbᵥ, and Iᵥ are only electron trap states and Iᵥ has a hole trap state, while MAᵥ could be an e-h recombination center but with a weak recombination rate. In addition, the NAC for the direct recombination path is similar or smaller than that of the pristine system. These conclusions are also collaborated by the orbital distribution that includes the effect of SOC shown in fig. S2.

**DISCUSSION**

It is useful to contrast MAPbI₃ with a traditional semiconductor such as TiO₂. The by-defect e-h recombination process shown in Fig. 3 is also active in TiO₂. However, in strong contrast to TiO₂, in MAPbI₃, the rates are not accelerated as compared with the pristine system. In rutile TiO₂, Zhang et al. (33) showed that non-isoelectronic Cr-N substitutions for Ti-O would induce a delocalized impurity phonon mode (section S7) with strong coupling with neighboring atoms, which notably enhances the NAC from 1.5 meV for the undoped system to ~25 meV. On the other hand, for isoelectronic V-N co-doped substitution, the impurity phonon modes are localized, and the recombination rates are not different from the undoped system. Similar analysis on the phonon localization in our system, as seen in figs. S5 and S6, shows that defect-related atoms have 20% contributions to different phonon modes. This is indicative that the defect-related phonon modes that couple to the electron subsystem are also delocalized, which is similar to the non-isoelectronic doping in TiO₂. However, in contrast to the TiO₂ systems, the NAC for the MAPbI₃ systems is not enhanced, and hence, we do not see an acceleration of the e-h recombination. The main reason for the differences with TiO₂, and consequently for the strong defect tolerance in MAPbI₃, is that the phonon modes that drive the NAC have relatively low frequencies below 100 cm⁻¹, as shown in Fig. 4. In contrast, in pristine TiO₂, the CBM and VBM couple with phonons above 500 cm⁻¹, while the defect states couple with impurity phonons above 900 and 800 cm⁻¹ for the isoelectronic and non-isoelectronic substitutions, respectively (33).
The notable differences in the phonons between TiO₂ and MAPbI₃ can be correlated with their bulk moduli. The bulk modulus of MAPbI₃ is smaller than typical metal oxides like TiO₂ by one order of magnitude (41–45). The bulk modulus is determined by the second derivative of the energy of the system versus the volume change, which makes it sensitive to the lattice phonon modes (46, 47). In MAPbI₃, the small bulk modulus can be attributed to the low-frequency phonon modes of the inorganic lattice. We propose that the “soft” nature (small bulk moduli) of MAPbI₃ is correlated with the weak NAC and hence prolonged e-h recombination lifetimes. These conclusions are likely applicable to other semiconductors with small bulk moduli including other hybrid organic-inorganic perovskites.

For completeness, the defect tolerance in MAPbI₃ could also be due to additional factors such as the formation of large polarons, as well as reduced Coulomb screening based on local symmetry breaking and dynamic ferroelectric effect (18, 42, 43, 44, 48, 49). As argued recently, on the basis of direct time-domain view, large polarons form in MAPbBr₃ and CsPbBr₃ due to deformations in Ptb₃ lattice regardless of the cation, which is also in line with our findings that the organic molecule has little effect, if any, on the NAC. In addition, recently, Meggiolaro et al. (17) argued that the peculiar iodine redox chemistry could explain the defect tolerance, as this will promote faster hole trapping compared to electron trapping.

The NAMD simulation results of MAPbI₃ are not consistent with the well-known SRH mechanism proposed in the 1950s (21), which has been widely used to predict the e-h recombination rates based on the electronic structures of defects (section S6). By only considering the carrier concentration and the energy of the defect state, SRH predicts that deep defect states in the middle of the band gap behave as an e-h recombination center. On the contrary, if the defect states are close to the VBM or CBM, then the electron/hole will be easily trapped, and charge recombination will not be accelerated. Here, our results show that charge recombination is not accelerated in the presence of native defects regardless of the location of the defect state in the band gap. As we showed in this study, the breakdown of SRH is because the electron-phonon coupling, which is the dominating factor of the nonradiative charge recombination, is not considered in the original SRH model. Our results suggest that in halide perovskites, the coupling with the low-frequency lattice phonons efficiently suppresses the charge recombination and the simple SRH model is not sufficient. These findings call for careful time-resolved experimental measurements to benchmark different theoretical methods and models.

To summarize, using time-dependent ab initio NAMD simulation, we have investigated the e-h recombination dynamics of five stable native point defects in MAPbI₃. Although the electronic structure associated with the defect states is distinct in these different systems, we have not observed the acceleration of charge recombination. On the contrary, 1 suppresses the e-h recombination. Our analyses show that the strong defect tolerance in MAPbI₃ is due to the low-frequency phonons contributed by the inorganic lattice that are weakly coupled to the organic molecules. In MAPbI₃, only low-frequency phonon modes can be excited, resulting in a weak NAC between the states. We propose that these conclusions are also applicable to other hybrid perovskites, which share with MAPbI₃ similar properties, in particular, a small bulk modulus value. These findings are important in the future design of functional semiconducting materials for solar energy conversion.

MATERIALS AND METHODS
The ab initio NAMD simulations were performed using the Hefei-NAMD code (33, 34, 50, 51) within real-time time-dependent KS equation framework (34). We used VASP (Vienna Ab initio Simulation Package) (52) to optimize the structure at T = 0 K, obtain the nuclear trajectory, and calculate the KS orbitals that are needed to compute the NAC for NAMD simulations. The electron-nuclei interactions were described using the projector augmented-wave method (53). The tetragonal phase is represented using a (\(\sqrt{2} \times \sqrt{2} \times 2\)) unit cell of the cubic phase with lattice constants a = 8.8 Å and c = 12.685 Å. We used a 4 \times 4 \times 4 Monkhorst-Pack k-point mesh to sample the Brillouin zone. After the geometry optimization, we used velocity rescaling to bring the system’s temperature to 300 K; a 10-ps microcanonical ab initio MD trajectory was then generated with a time step of 1 fs. Using the MD trajectory, the NAMD results were based on averaging over 100 different initial configurations. For each chosen structure, we sampled 500 trajectories for 2 ns. Decoherence-induced surface-hopping method was used to account for quantum decoherence (section S5) (54). In general, shorter decoherence time leads to slower dynamics, as exemplified by the quantum Zeno effect in which the dynamics stop in the limit of infinitely fast decoherence (55).

The density functional theory (DFT) calculations PBE (56) exchange-correlation functional and accounts for van der Waals interactions that are important for MHP systems (36) using DFT-D3 (57). Because of the presence of heavy Pb atoms, the inclusion of SOC is important to correctly describe the band structure (58) and even the stability (7) of MAPbI₃. Because semi-local functionals generally underestimate the band gap, previous studies have shown that PBE without SOC yields band gaps in good agreement with experiments and high-level SOC + GW calculations due to a cancelation of the two effects (59). NAMD investigations are computationally expensive, requiring solving KS equations a few thousand times. Thus, it is not practical to use SOC + GW calculations in the NAMD simulations. Instead, here, we simply used the PBE functional as performed in previous NAMD studies on MAPbI₃ (30, 31). However, given the importance of SOC corrections, we further used calculations with SOC to assess their impact on our results (section S3). In addition, we investigated the effects of using the hybrid exchange-correlation functional HSE06 with 43% exact exchange, as proposed in (17). When coupled to SOC, this modified HSE06 yields electronic structure similar to the high-level GW-SOC (59). The NAC values obtained with PBE-SOC and HSE06-SOC are summarized in tables S1 and S2.

In NAMD simulations, the NAC was numerically evaluated from the overlap between two KS orbitals at adjacent ionic time steps (40). Because the adiabatic KS orbitals along the trajectory can differ by an arbitrary random phase due to the different mathematical methods, the overlap of the KS orbitals is not uniquely determined, which leads to a “phase consistency” problem. If not accounted for correctly, then this random phase will result in an erroneous evaluation of the NAC and subsequently cause serious problems in the numerical integration of the NAMD equations, making the NAMD results not reproducible. In our calculations, we applied the phase correction similar to the method introduced by Akimov (60).

SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/6/7/eaaw7453/DC1
Section S1. Impurity concentration
Section S2. Spin-orbit coupling
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