ELLA: Exploration through Learned Language Abstraction

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Abstract

Building agents capable of understanding language instructions is critical to effective and robust human-AI collaboration. Recent work focuses on training these agents via reinforcement learning in environments with synthetic language; however, instructions often define long-horizon, sparse-reward tasks, and learning policies requires many episodes of experience. We introduce ELLA: Exploration through Learned Language Abstraction, a reward shaping approach geared towards boosting sample efficiency in sparse reward environments by correlating high-level instructions with simpler low-level constituents. ELLA has two key elements: 1) A termination classifier that identifies when agents complete low-level instructions, and 2) A relevance classifier that correlates low-level instructions with success on high-level tasks. We learn the termination classifier offline from pairs of instructions and terminal states. Notably, in departure from prior work in language and abstraction, we learn the relevance classifier online, without relying on an explicit decomposition of high-level instructions to low-level instructions. On a suite of complex BabyAI [11] environments with varying instruction complexities and reward sparsity, ELLA shows gains in sample efficiency relative to language-based shaping and traditional RL methods.

1 Introduction

A long-standing goal for robotics and embodied agents is to build systems that can perform tasks specified in natural language [1, 8, 21, 26, 39, 42, 43]. Central to the promise of language is its ability to cleanly specify complex, multi-step instructions. Instructions like make a cup of coffee define long-horizon tasks as abstractions over lower-level components—simple instructions like pick up a cup or turn on the coffee maker. Leveraging these abstractions can help amplify the sample efficiency and generalization potential of our autonomous agents.

One way to do this is through the lens of instruction following, which can be framed in several ways. One common framing—and the one we use in this work—is via reinforcement learning (RL): an agent is given a start state, a language instruction, and a corresponding reward function to optimize that usually denotes termination [21, 31]. While RL can be a useful framing, such approaches are often not sample efficient [11, 21]. Especially in the case of complex, highly compositional language instructions, RL agents can fail to make progress quickly—or at all. There are several reasons for poor performance in these settings; paramount is that in many environments, these instructions are...
In this example, an expert provides examples of when low-level *go to* tasks are and are not solved, and the agent trains a termination classifier. During policy learning, the agent rewards itself for completing *go to* subtasks—specifically, those which are relevant to its current high-level task. It stores successful experiences to learn to correlate low-level *go to* tasks with high-level *put next* tasks.

tied to sparse reward functions that only provide signal upon completion of the high-level task, which drastically hurts sample efficiency. For example, seeing reward for *make a cup of coffee* would require already having turned on the coffee maker, which could itself be a difficult task. Such “bottleneck” states, which have zero intermediate reward, complicate exploration and learning [30, 40].

Our goal is to improve sample efficiency for instruction following agents operating in sparse reward settings. Driving our approach is using the principle of abstraction—the fact that complex instructions entail simpler ones—to guide exploration. Consider our coffee example; we would like to guide the agent to explore in a structured fashion, learning low-level behaviors first (*pick up a cup, turn on the coffee machine*) and building up to solving the high-level task. To do this, we frame our problem via reward shaping, the general technique of supplying auxiliary rewards to guide learning [32, 36].

Our approach, Exploration through Learned Language Abstraction (ELLA) provides intermediate rewards to an agent for completing relevant low-level behaviors as it tries to solve a complex, sparse reward task. Notably, our approach 1) learns to identify the low-level primitives helpful for a high-level language task *online*, and 2) does not require a strict hierarchical decomposition of language instructions to these primitives. Rather, ELLA uses low-level instructions to support agents performing complex tasks, bonus agents as they complete *relevant* behaviors. In contrast to prior work [3, 24] that assumes strict contracts over instruction decomposition, our contract is simple and general. This prior work assumes each high-level task is comprised of exact series of low-level policies—an assumption that is only possible when the full set of primitives is known ahead of time, and fails when new actions or further exploration are necessary.

In order to bonus agents as they complete relevant subtasks, ELLA assumes access to a set of low-level instructions and corresponding termination states, similar to the data assumed in prior work [6]. While collecting such data for complex tasks may require time and effort, annotations for low-level instructions are more tractable. Humans can quickly annotate instructions like *pick up the cup* or *open the cupboard*, or even build tools for generating such examples. This is increasingly apparent in prior work [5, 23, 26, 44]: low-level instructions are used to simplify the problem of interpreting high-level instructions, through a variety of mechanisms. In our case, these low-level instructions provide the basis for reward shaping.

We empirically validate our abstraction-based reward shaping framework on a series of tasks via the BabyAI platform [11]. We compare against a standard RL baseline as well as to a strong language-based reward shaping approach [17], and find that our method leads to substantial gains in sample efficiency across a variety of instruction following tasks.
2 Related Work

We build on a large body of work that studies language in the context of reinforcement learning (RL) [28] with a focus on methods for instruction following, leveraging hierarchy, and reward shaping.

**Instruction Following.** Instruction following focuses on the automated execution of language commands in simulated or real environments [1, 16, 27, 42, 45]. We focus on the RL setting [11, 31], where agents learn language-conditioned policies in a Markov decision process (MDP).

Even simple instruction following problems are difficult to learn [29], which has made 2D environments important test-beds for new learning methods [3, 11, 47]. Such environments, which are procedurally-generated, are useful because they decouple exploration from the problem of perception, and demand policies that do not overfit to narrow regions in the state space [10, 13].

We use BabyAI [11] as the platform for our tasks. BabyAI’s language is synthetic, similar to prior work examining RL for instruction following at scale [21, 22]. These environments are scalable starting points for new instruction following approaches, since deep RL remains sample-inefficient but has the potential to flexibly deal with complex environments [22]. Simplified environments also make investigating concepts such as language abstraction possible, and these concepts can generalize to real human-AI interactions [26, 44]. We describe our experimental setup in Section 5.

**Hierarchical and Language-Structured Policies.** A large body of work in hierarchical RL studies temporal abstractions of MDPs, where policies are designed or learned at multiple levels of hierarchy [41]. Recent works have made the connection to language: for example, high-level policies can act over the space of low-level instructions [24]. Other hierarchical language techniques include learning models that predict symbolic representations of reward functions at different granularities [5, 25], and compositional approaches like policy sketches [3] and modular control [15], methods that explicitly decompose high-level instructions into sequences of predefined low-level instructions, or subtasks.

In this work, we use language hierarchically, but without the strict decomposition assumption made by prior work: we do not assume high-level tasks are composed of an exact series of low-level tasks. Without this assumption, it is infeasible to use explicitly modular approaches [3, 5, 15]. A further distinguishing factor of our method relative to prior work is that we do not require high-level task decompositions be provided a priori. We expand on these features in Section 3.

**Language and Reward Shaping.** Reward shaping is a general technique for supplying auxiliary rewards in order to guide an agent’s learning process. Certain types of reward transformations, such as potential-based rewards, do not change the optimal policy but can impact sample efficiency [32]. Prior work has applied reward shaping to language-based instruction following settings. Goyal et al. [17] train a classification network on (trajectory, language) data to predict if a trajectory (parameterized by action frequencies) matches a language description, and evaluate the network at every time step to form a potential-based reward shaping function. They evaluate their method on Montezuma’s Revenge, which is a complex task, but with a static, deterministic layout that does not speak to the generalization potential of such methods. Relatedly, Waytowich et al. [46] use a narration-based approach, where high-level tasks are explicitly broken down into low-level tasks as narrations. Finally, Misra et al. [31] use a shaping function based on spatial distance to goals specified in language, but require the location of the goal to be known. In this work, we use the same high level principle—language can yield useful intermediate rewards—but do not make the restrictive assumptions of prior work about the environment or the way tasks are structured.

**Other Forms of Guidance.** Several other methods exist for improving the sample efficiency of RL in sparse reward settings. These methods reward an aspect of exploration that is orthogonal to our approach, and we see potential for combining these methods with ours. One popular technique is hindsight experience replay (HER), in which failed trajectories are stored in a replay buffer and relabeled with new goals that get nonzero reward [4]. Jiang et al. [24] extend the method to hierarchical language settings, assuming a mapping from states to corresponding goals. Cideron et al. [12] learn this mapping alongside policy training using the environment reward as supervision. Another technique for improving sample efficiency is through intrinsic motivation [9, 33, 35, 37]. In general, these methods instantiate reward shaping to incentivize accessing novel, diverse, or unpredictable parts of the state space via intrinsic rewards, and they can be extended to language-
conditioned settings as well [14]. In Appendix D, we evaluate the performance of RIDE [35], an intrinsic motivation method that rewards actions that cause significant changes to the state, and discuss potential synergies with ELLA.

3 Problem Statement

We consider an augmented MDP $M$ defined by the tuple $(S, A, T, R, G, \gamma)$ where $S, A, T, \text{ and } \gamma$ are standard. $A$ consists of primitive actions—in BabyAI, these are navigation primitives (forward, pick up, etc.). $G$ is a set of language instructions, from which a high-level task instruction $g$ is drawn, and $R : S \times A \times G \rightarrow [0, 1]$ represents the state-action reward given some $g$. Via RL, we wish to find some policy $\pi : S \times G \rightarrow A$ that maximizes the expected discounted return.

We specifically consider cases where $M$ has a finite horizon $H$ and $R$ is sparse with respect to goal-completion, making exploration difficult. Our aim is to construct a reward transformation $R \rightarrow R'$ which is policy invariant with respect to the original MDP (i.e., an optimal policy for $M' = (S, A, T, R', g, \gamma)$ is also optimal in $M$ and vice versa), while providing the agent strong signal conducive to sample-efficient exploration.

We assume access to a set of low-level instructions $G_{ll}$ such that every $g \in G$ is supported by some $g_{ll} \in G_{ll}$. Note that we do not require that high-level tasks fully factorize into low-level tasks. To clarify the distinction, say that $G_{ll}$ consists of go to “x” instructions: go to the red ball, go to the blue ball, etc. The instruction go to the red ball and then go to the blue ball can be fully factorized into low-level tasks in $G_{ll}$. On the other hand, the instruction put the red ball next to the green key is supported by go to the red ball, but it also requires picking up and putting down the ball—actions not covered by $G_{ll}$. Our framing permits exploration using a mixture of low-level instructions as well as primitive actions in $A$ (such as pick up and put down).

We assume that examples of the corresponding termination states of instructions in $G_{ll}$ are easy to obtain—via a human expert or automation. This is reasonable for simple low-level tasks like the go to tasks in Figure 1. However, it is less feasible in domains where data collection is costly and the environment is hard to simulate; we address this further in Section 7.

Our code is available at https://github.com/Stanford-ILIAD/ELLA.

The environments in our experiments are partially observable, so we use recurrent networks that ingest sequences of observations $(o_1, o_2, \ldots, o_t)$ rather than a single state $s_t$ [20]. Though our notation describes the fully observable setting, the extension to the partially observable case is straightforward.

4 ELLA

We present ELLA, our reward shaping framework for guiding exploration using learned language abstractions.1 Figure 1 provides a graphical overview of ELLA. Our approach rewards an agent when it has completed low-level tasks that support a given high level task. To do this, it predicts 1) when a low-level task terminates and 2) when a low-level task is relevant. Section 4.1 describes our low-level termination classifier. Section 4.2 describes our relevance classifier, and how we learn it online during RL. Finally, Section 4.3 details our reward shaping scheme, which bonuses an agent for exploring states that satisfy relevant low-level tasks.

4.1 Learning the Low-Level Termination Classifier

We train a binary termination classifier $h^{\phi} : S \times G_{ll} \rightarrow \{0, 1\}$ parameterized by $\phi$ to predict if a low-level task $g_{ll} \in G_{ll}$ terminates in a particular state $s \in S$. We assume access to $G_{ll}$ as well as positive and negative examples of low-level task termination states. This dataset could be annotated by a human or created automatically. While providing demonstrations of high-level tasks (e.g., make a cup of coffee) across varied environments is costly, it is more feasible to do so for low-level tasks (e.g., pick up the mug) which are shorter, simpler, and more generalizable. To represent $h^{\phi}$, we adapt the architecture from [11] which merges state and language representations using feature-wise linear modulation (FiLM) [34].
Algorithm 1 Reward Shaping via ELLA

Input: Initial policy parameters \( \theta_0 \), relevance classifier parameters \( \rho_0 \), update rate \( \eta \), low-level bonus \( \lambda \), and RL optimizer \( \text{OPTIMIZE} \)

Initialize \( D \leftarrow \{ (g : G) \text{ for all } g \in G \} \)

for \( k = 0, 1, \ldots \) do

Collect trajectories \( D_k \) using \( \pi_k^\phi \).

for \( \tau \in D_k \) do

Set \( N \leftarrow \text{length of } \tau \).

if \( U(\tau) > 0 \) then

Set \( r_N' \leftarrow \text{NEUTRALIZE}(r_{1:N}) \).

Update \( \theta_{k+1} \leftarrow \text{OPTIMIZE}(r_{1:N}') \).

if \( k \) is a multiple of \( n \) then

Update \( \rho_{k+1} \) by optimizing cross entropy loss on a balanced sample from \( D \).

end

end

function \( \text{SHAPE}(\tau) \)

Set \( \hat{S} \leftarrow \emptyset \)

for \( g_t \in G \) do

for \( (s_t, r_t) \in \tau \) do

if \( h^\phi(s_t, g_t) = 1 \) and \( g_t \notin \hat{S} \) then

Update \( \hat{S} \leftarrow \hat{S} \cup \{ g_t \} \).

end

end

end

return \( (r_1', \hat{S}) \).

function \( \text{NEUTRALIZE}(r_{1:N}) \)

Set \( T_{\hat{S}} \leftarrow \{ t \mid 1 \leq t \leq N, r_t' > 0 \} \).

return \( r_N' - \sum_{t \in T_{\hat{S}}} r_t' \).

function \( \text{UPDATEDECOMP}(D, \hat{S}) \)

Set \( S \leftarrow D \left| g \right| \).

return \( S \cap \hat{S} \) (or \( S \) if \( S \cap \hat{S} = \emptyset \)).

4.2 Learning the Relevance Classifier

Our reward shaping approach also needs to evaluate relevance of a low-level instruction in addition to being able to classify termination. The relevance mapping from \( G \) to \( \mathcal{P}(G_t) \) (the power set of \( G_t \)) is initially unknown to the agent. We refer to the output of this mapping as a decomposition of \( g \), but note again that it need not be a strict decomposition. We propose that this mapping is represented by a separate binary relevance classifier \( f^\rho : G \times G_t \to \{ 0, 1 \} \) learned during policy training from a dataset of decompositions \( D \) collected online. The output of \( f^\rho \) indicates whether a particular \( g_t \in G_t \) is relevant to some \( g \in G \). We use a Siamese network to represent \( f^\rho \).

Training the Relevance Classifier. Suppose \( D \) already contains key-value pairs \( (g, S) \) where \( g \in G \) and \( S \in \mathcal{P}(G_t) \). Each \( S \) is an estimate of the oracle decomposition \( \hat{S} \) of a particular \( g \). For every \( g \) in \( D \), we enumerate negative examples of relevant subtasks from \( G_t \setminus S \) and accordingly oversample positive examples from \( S \); then optimize a cross entropy objective on this balanced dataset.

Collecting Relevance Data Online. We describe any trajectory that solves the high-level task as successful, regardless of whether they do so optimally, and any other trajectories as unsuccessful. For every successful trajectory of some \( g \) we encounter during RL training, we record the low-level instructions which terminated. That is, we relabel the steps in the trajectory and use \( h^\phi \) to determine which low-level instructions were completed (if any), yielding an estimate \( \hat{S} \) of the true decomposition \( S \). If \( D \) already contains an estimate \( S \) for \( g \), we simply deduplicate the multiple decomposition estimates by intersecting \( S \) and \( \hat{S} \). As the agent completes more successful trajectories, decompositions in \( D \) are more likely to get revisited.

Intuition for Deduplication. Intuitively, this method for deduplication denoises run-specific experiences, and distills the estimate \( S \) in \( D \) for a given \( g \) to only those \( g_t \) that are shared among multiple successful runs of \( g \). Consider \( g = \text{put the red ball next to the blue box} \); successful runs early in training could highlight go to the red ball along with irrelevant go to low-level instructions. As \( \pi^\phi \) improves, so do the decomposition estimates. Later runs may highlight only go to the red ball. Taking the intersection would yield only go to the red ball as our final estimate \( \hat{S} \). This approach also helps to deal with false positives of \( h^\phi \) by effectively boosting the estimate across runs. If deduplication produces a null intersection, which may happen due to false negatives of \( h^\phi \), we err on the side of using the latest estimate. If we assume \( h^\phi \) has perfect accuracy, the intersection will never be null, and the continual intersections will reflect the set of completed \( g_t \) common to all successful runs of \( g \). For an initialization conducive to deduplication and that provides \( \pi^\phi \) strong incentive to complete low-level tasks from the beginning of training, we initialize \( f^\rho \) to predict that \( S = G_t \) for all \( g \).
We establish two desiderata for $R$ which relies on $h$ and $f$. $R'$ provides a bonus $\lambda$ whenever a relevant low-level task terminates. We do this by relabeling the current $(s_t, a_t, r_t, s_{t+1})$ with every $g_t$ and using $h$ to predict low-level task termination, and $f$ to predict relevance.

Critically, we do not want the shaping transformation from $R \to R'$ to be vulnerable to the agent getting “distracted” by the shaped reward (reward hacking), as in Randløv and Alstrøm [36] where an agent learns to ride a bicycle in a circle around a goal repeatedly accruing reward. To this end, we cap the bonus per low-level instruction per episode to $\lambda$ to prevent cycles. More generally, we want $R'$ to be policy invariant with respect to $\mathcal{M}$: it should not introduce any new optimal policies, and it should retain all the optimal policies from $\mathcal{M}$. Policy invariance is a useful property [32]: we do not want to reward a suboptimal trajectory (such as one that repeatedly completes a low-level instruction) more than an optimal trajectory in $\mathcal{M}$, and policy invariance guarantees this.

We establish two desiderata for $R'$ [7]: (a) The reward transformation should be policy invariant with respect to $\mathcal{M}$ for states from which the task is solvable, and (b) $R'$ should improve sample efficiency by encouraging subtask-based exploration. To satisfy our desiderata, we choose $R'$ such that successful trajectories get the same return under $\mathcal{M}$ and $\mathcal{M}'$, and that unsuccessful trajectories get lower returns under $\mathcal{M}'$ than trajectories optimal in $\mathcal{M}$. We will describe and intuitively justify each of these choices with respect to (a) and (b).

**Neutralization in Successful Trajectories.** We neutralize shaped reward in successful trajectories—that is, subtract the shaped reward at the final time step—so that successful trajectories get the same return under both $R'$ and $R$.

More specifically, let $U(\tau) := \sum_{t=1}^{N} \gamma^t R(s_t, a_t)$, the cumulative discounted return under $R$ of a successful trajectory $\tau$. Let $U'(\tau)$ be likewise defined for $R'$. If $\tau$ has $N$ steps, the sparse reward under $R$ is $U(\tau) = \gamma^N r_N$. Under $R'$, if $T_\lambda$ is the set of the time steps at which a $\lambda$ bonus is applied, we set $r'_N$ to $r_N - \sum_{t \in T_\lambda} \gamma^{t-N} \lambda$. This is the value required to neutralize the intermediate rewards, such that $U'(\tau) = \gamma^N r'_N = U(\tau)$ (Note that we cap the bonus per time step to $\lambda$—if multiple low-level language instructions terminate at a single state, only a bonus of $\lambda$ is applied.)

Theoretically, we could apply neutralization to all trajectories, not just successful ones, and we would satisfy property (a) [19]. However, this is harmful to property (b), because unsuccessful trajectories would result in zero return: a negative reward at the last time step would negate the subtask rewards, potentially hurting boosts in sample efficiency.

### Table 1: Sample low- and high-level instructions.

| Low-Level Task | Example | $g_t$ |
|----------------|---------|-------|
| GO-TO-ROOM (G1) | go to a purple ball | |
| GO-TO-MAZE (G2) | go to a purple ball | |
| OPEN-MAZE (O2) | open the red door | |
| PICK-MAZE (P2) | pick up the blue box | |

| High-Level Task | Example(s) | $g_t$ |
|-----------------|------------|-------|
| PUTNEXT-ROOM    | put the purple ball next to the key | G1 |
| PUTNEXT-MAZE    | put the purple ball next to the key | G2 |
| UNLOCK-MAZE     | open the green door | P2 |
| OPEN&PICK-MAZE  | open the red door and pick up the blue box | O2, G2 |
| COMBO-MAZE      | put next, open, pick | G2 |
| SEQUENCE-MAZE   | pick up a purple key and then put the grey box next to the red box | G2 |

4.3 Shaping Rewards

We now describe the shaped reward function $R'$ which relies on $h$ and $f$. $R'$ provides a bonus $\lambda$ whenever a relevant low-level task terminates. We do this by relabeling the current $(s_t, a_t, r_t, s_{t+1})$ with every $g_t$ and using $h$ to predict low-level task termination, and $f$ to predict relevance.

We neutralize shaped reward in successful trajectories—that is, subtract the shaped reward at the final time step—so that successful trajectories get the same return under both $R'$ and $R$.

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Theoretically, we could apply neutralization to all trajectories, not just successful ones, and we would satisfy property (a) [19]. However, this is harmful to property (b), because unsuccessful trajectories would result in zero return: a negative reward at the last time step would negate the subtask rewards, potentially hurting boosts in sample efficiency.
We used a combination of NVIDIA Titan and Tesla T4 GPUs to train our models. We ran 3 seeds for each of the 3 methods in each environment, with runs taking 1 to 6 days.

Results. Figure 2 presents learning curves for ELLA, LEARN, and PPO (without shaping) across the six environments. We explain our results in the context of the three axes described above.

→ How does ELLA perform on tasks with different degrees of sparsity?

In both single room (PUTNEXT-ROOM) and two room (PUTNEXT-MAZE) environments, ELLA induces gains in sample efficiency, using GOTo as $G_t$. Relative gains are larger for the bigger...
environment because reward signals are more spatially sparse and so spatial subgoals—visiting relevant objects—help the agent navigate.

Another degree of sparsity comes from bottleneck states: for example, in the UNLOCK environment, the agent must pick up a key of the corresponding color (the bottleneck) before it can successfully open a colored door and see reward. Without shaping, random exploration rarely passes such bottlenecks. However, in this experiment, ELLA rewards picking up keys, via the PICK low-level instruction, quickly learning to correlate picking up keys of the correct color with successfully unlocking doors, allowing agents to navigate these bottlenecks and improving sample efficiency.

→ *How does ELLA perform when the low-level tasks are similar to the high-level task?*

Tasks in the COMBO environment consist of multiple instruction types (e.g., *put the red ball next to the green box*, *open the green door*, and *pick up the blue box*). The latter instructions require minimal exploration beyond “going to” an object — such as executing an additional open or pick up primitive actions. That is, the low-level task GOTo is more similar to this high-level task set than in the other environments such as PUTNEXT. As a result, ELLA does not increase in sample efficiency in COMBO. However, it notably does not perform worse than baselines: the exploration it encourages is not harmful, but is simply not helpful. This is expected as achieving the COMBO tasks is about as difficult as exploring the relevant GOTo subtasks.

→ *How does ELLA perform when the high-level tasks are compositional and diverse?*

We test ELLA on OPEN&PICK using two low-level instruction families, OPEN and GOTo. The instruction *open the yellow door and pick up the blue box* abstracts over *go to the yellow door*, *open the yellow door*, and *go to the blue box*. Although learning $f^p$ becomes harder with more compositional instructions, the boost in sample efficiency provided by ELLA remains.

Similarly, SEQUENCE has a combinatorially-large number of compositional instructions: it requires two of *put next*, *open*, and *pick up* in the correct order. It has over 1.5 million instructions compared to the other high-level tasks with 300 to 1500 instructions. Although the exploration problem is very difficult, we see marginal gains from ELLA; we discuss this further in Section 7.
6 Analyzing ELLA

In this section, we analyze two aspects of ELLA: the effect of different choices for the low-level reward hyperparameter (Section 6.1), and the performance of the relevance classifier (Section 6.2).

6.1 Effect of the Low-Level Task Reward

The magnitude of the low-level reward $\lambda$ is a critical hyperparameter. Instead of using ad hoc methods for tuning $\lambda$, Section 4.3 provides guidelines for choosing a reasonable range for $\lambda$. To summarize, we want to pick $\lambda$ small enough that any unsuccessful trajectory does not receive greater return than any optimal trajectory. In this section, we examine PUTNEXT-ROOM and evaluate various $\lambda$ values determined using the multi-tier assumptions alluded to in Section 4.3. For this task, we have that $H = 128$ and $|G_t| = 36$. With no knowledge of the environment or optimal policy, the loosest bounds for $M$ and $|T_5|$ ($H$ and $|G_t|$ respectively), as in (1) yield $\lambda = 0.015$. With the minimal assumption that an optimal policy solves the task in under 100 steps, we arrive at $\lambda = 0.05$. For 40 steps, we arrive at $\lambda = 0.25$. Figure 3 compares learning curves for $\lambda$—the smallest being more conservative and not having a great effect on sample efficiency, the middle values illustrating the value of rewarding relevant subtasks, and the largest values chosen specifically to demonstrate that egregious violations of policy invariance can “distract” the agent from the high-level task and lead to unstable learning. The results in Section 5 use $\lambda=0.25$ for PUTNEXT, UNLOCK, and COMBO, and use $\lambda=0.5$ for OPEN&PICK and SEQUENCE (which have longer horizons $H$).

6.2 Progress of the Relevance Classifier

The online relevance dataset and classifier provide transparency into the type of guidance that ELLA provides. Figure 4 focuses on PUTNEXT-MAZE and SEQUENCE-MAZE, and shows two metrics: the average number of subtasks per high-level instruction in $D$, which we expect to decrease as decomposition estimates improve; and the validation accuracy of $f^\rho$ in classifying a balanced oracle set of subtask decompositions, which we expect to increase if ELLA learns language abstractions.

For PUTNEXT-MAZE, the number of subtasks per high-level instruction decreases and the relevance classifier becomes very accurate. This happens as, from Figure 2, the policy improves in terms of average return. For the SEQUENCE-MAZE task, ELLA has marginal gains in performance compared to baselines (Figure 2). This is likely due to ELLA incentivizing general subtask completion, evidenced by the growing average length of the decompositions. However, the large number of diverse language instructions in SEQUENCE-MAZE makes it difficult to estimate good decompositions via our deduplication method (as it is uncommon to see the same instruction multiple times). It is difficult to learn $f^\rho$ online and offer the most targeted low-level bonuses in this case.
7 Discussion

We introduce ELLA, a reward shaping approach for guiding exploration based on the principle of abstraction in language. Our approach incentivizes low-level behaviors without assuming a strict hierarchy between high- and low-level language, and learns to identify relevant abstractions online.

As noted in Section 2, several other methods exist for addressing sample inefficiency in sparse reward settings. While we focus on using language as the basis for reward shaping, intrinsic rewards can also be based on the dynamics of the environment. For example, RIDE [35] provides rewards for actions that produce significant changes to the state. In Appendix D, we discuss how ELLA can synergize with such methods to reward different aspects of exploration.

Limitations and Future Work. Our framework requires termination states for each low-level instruction. This assumption is similar to that made by Jiang et al. [24] and Waytowich et al. [46], and is weaker than the assumption made by the LEARN baseline of Goyal et al. [17], where full demonstrations are required. Even so, training accurate termination classifiers can require many examples—in this work, we used 15K positive and negative pairs for each low-level task. In Appendix E, we provide an ablation on the data budget for the termination classifier. Our approach is less feasible in domains where collecting examples of low-level terminating conditions is costly.

Highly compositional and diverse instructions, as in the SEQUENCE-MAZE environment, remain a challenge. Data augmentation (e.g., GECA [2]) on the online relevance dataset could potentially improve performance on these large instruction sets. Additional boosts in performance and generalization could emerge from instilling language priors via offline pre-training: More sophisticated relevance classifiers may also prove helpful: instead of deduplicating and training on \( D \), we could maintain a belief distribution over whether high- and low-level instructions are relevant conditioned on trajectories observed online. Furthermore, the relevance classifier could be extended to model the temporal order of the low-level tasks.

Our approach shows strong performance in several sparse reward task settings with synthetic language. Extensions to natural language could model a broad spectrum of abstraction beyond two tiers.

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References

[1] P. Anderson, Q. Wu, D. Teney, J. Bruce, M. Johnson, N. Sünderhauf, I. Reid, S. Gould, and A. van den Hengel. Vision-and-language navigation: Interpreting visually-grounded navigation instructions in real environments. In Computer Vision and Pattern Recognition (CVPR), 2018.

[2] J. Andreas. Good-enough compositional data augmentation. In Association for Computational Linguistics (ACL), 2020.

[3] J. Andreas, D. Klein, and S. Levine. Modular multitask reinforcement learning with policy sketches. In International Conference on Machine Learning (ICML), 2017.

[4] M. Andrychowicz, F. Wolski, A. Ray, J. Schneider, R. Fong, P. Welinder, B. McGrew, J. Tobin, P. Abbeel, and W. Zaremba. Hindsight experience replay. arXiv preprint arXiv:1707.01495, 2017.

[5] D. Arumugam, S. Karamcheti, N. Gopalan, L. L. S. Wong, and S. Tellex. Accurately and efficiently interpreting human-robot instructions of varying granularities. In Robotics: Science and Systems (RSS), 2017.

[6] D. Bahdanau, F. Hill, J. Leike, E. Hughes, S. A. Hosseini, P. Kohli, and E. Grefenstette. Learning to understand goal specifications by modelling reward. In International Conference on Learning Representations (ICLR), 2019.
[7] P. Behboudian, Y. Satsangi, M. E. Taylor, A. Harutyunyan, and M. Bowling. Usef ul policy invariant shaping from arbitrary advice. arXiv preprint arXiv:2011.01297, 2020.

[8] Y. Bisk, A. Holtzman, J. Thomason, J. Andreas, Y. Bengio, J. Chai, M. Lapata, A. Lazaridou, J. May, A. Nisnevich, N. Pinto, and J. Turian. Experience grounds language. In Empirical Methods in Natural Language Processing (EMNLP), 2020.

[9] Y. Burda, H. Edwards, D. Pathak, A. Storkey, T. Darrell, and A. A. Efros. Large-scale study of curiosity-driven learning. In International Conference on Learning Representations (ICLR), 2019.

[10] A. Campero, R. Raileanu, H. Küt tler, J. B. Tenenbaum, T. Rocktäschel, and E. Grefenstette. Learning with AMIGo: Adversarially motivated intrinsic goals. arXiv preprint arXiv:2006.12122, 2020.

[11] M. Chevalier-Boisvert, D. Bahdanau, S. La lhoul, W. Willems, C. Saharia, T. H. Nguyen, and Y. Bengio. BabyAI: A platform to study the sample efficiency of grounded language learning. In International Conference on Learning Representations (ICLR), 2019.

[12] G. Cideron, M. Seurin, F. Strub, and O. Pietquin. Self-educated language agent with hindsight experience replay for instruction following. In Advances in Neural Information Processing Systems (NeurIPS), 2019.

[13] K. Cobbe, C. Hesse, J. Hilton, and J. Schulman. Leveraging procedural generation to benchmark reinforcement learning. In International Conference on Machine Learning (ICML), 2020.

[14] C. Colas, T. Karch, N. Lair, J.-M. Dussoux, C. Moulin-Frier, P. F. Dominey, and P.-Y. Oudeyer. Language as a cognitive tool to imagine goals in curiosity driven exploration. In Advances in Neural Information Processing Systems (NeurIPS), 2020.

[15] A. Das, G. Gkioxari, S. Lee, D. Parikh, and D. Batra. Neural modular control for embodied question answering. In Conference on Robot Learning (CORL), 2018.

[16] J. Fu, A. Korattikara, S. Levine, and S. Guadarrama. From language to goals: Inverse reinforcement learning for vision-based instruction following. In International Conference on Learning Representations (ICLR), 2019.

[17] P. Goyal, S. Niekum, and R. J. Mooney. Using natural language for reward shaping in reinforcement learning. In International Joint Conference on Artificial Intelligence (IJCAI), 2019.

[18] Y. Goyal, U. Shalit, and B. Kim. Explaining classifiers with causal concept effect (CaCE). arXiv preprint arXiv:1907.07165, 2019.

[19] M. Grzes. Reward shaping in episodic reinforcement learning. In International Conference on Autonomous Agents and Multiagent Systems (AAMAS), 2017.

[20] M. Hausknecht and P. Stone. Deep recurrent Q-learning for partially observable MDPs. arXiv preprint arXiv:1507.06527, 2015.

[21] K. M. Hermann, F. Hill, S. Green, F. Wang, R. Faulkner, H. Soyer, D. Szepesvari, W. Czarnecki, M. Jaderberg, D. Teplyashin, M. Wainwright, C. Apps, D. Hassabis, and P. Blunsom. Grounded language learning in a simulated 3D world. arXiv preprint arXiv:1706.06551, 2017.

[22] F. Hill, S. Mokra, N. Wong, and T. Harley. Human instruction-following with deep reinforcement learning via transfer-learning from text. arXiv preprint arXiv:2005.09382, 2020.

[23] R. Jia and P. Liang. Data recombination for neural semantic parsing. In Association for Computational Linguistics (ACL), 2016.

[24] Y. Jiang, S. S. Gu, K. P. Murphy, and C. Finn. Language as an abstraction for hierarchical deep reinforcement learning. In Advances in Neural Information Processing Systems (NeurIPS), 2019.

[25] S. Karamcheti, E. C. Williams, D. Arumugam, M. Rhee, N. Gopalan, L. L. S. Wong, and S. Tellex. A tale of two dragons: A hybrid approach for interpreting action-oriented and goal-oriented instructions. In First Workshop on Language Grounding for Robotics @ ACL, 2017.

[26] S. Karamcheti, D. Sadigh, and P. Liang. Learning adaptive language interfaces through decomposition. In EMNLP Workshop for Interactive and Executable Semantic Parsing (IntEx-SemPar), 2020.

[27] T. Kollar, S. Tellex, D. Roy, and N. Roy. Toward understanding natural language directions. In Human-Robot Interaction, pages 259–266, 2010.
[28] J. Luketina, N. Nardelli, G. Farquhar, J. Foerster, J. Andreas, E. Grefenstette, S. Whiteson, and T. Rocktäschel. A survey of reinforcement learning informed by natural language. In *International Joint Conference on Artificial Intelligence (IJCAI)*, 2019.

[29] C. Lynch and P. Sermanet. Grounding language in play. *arXiv preprint arXiv:2005.07648*, 2020.

[30] A. McGovern and A. G. Barto. Automatic discovery of subgoals in reinforcement learning using diverse density. In *International Conference on Machine Learning (ICML)*, 2001.

[31] D. K. Misra, J. Langford, and Y. Artzi. Mapping instructions and visual observations to actions with reinforcement learning. In *Empirical Methods in Natural Language Processing (EMNLP)*, 2017.

[32] A. Y. Ng, D. Harada, and S. Russell. Policy invariance under reward transformations: Theory and application to reward shaping. In *International Conference on Machine Learning (ICML)*, volume 99, pages 278–287, 1999.

[33] D. Pathak, P. Agrawal, A. A. Efros, and T. Darrell. Curiosity-driven exploration by self-supervised prediction. In *Computer Vision and Pattern Recognition (CVPR)*, pages 16–17, 2017.

[34] E. Perez, F. Strub, V. Dumoulin, and A. C. Courville. FiLM: Visual reasoning with a general conditioning layer. In *Association for the Advancement of Artificial Intelligence (AAAI)*, 2018.

[35] R. Raileanu and T. Rocktäschel. RIDE: Rewarding impact-driven exploration for procedurally-generated environments. In *International Conference on Learning Representations (ICLR)*, 2020.

[36] J. Randløv and P. Alstrøm. Learning to drive a bicycle using reinforcement learning and shaping. In *International Conference on Machine Learning (ICML)*, 1998.

[37] J. Schmidhuber. Adaptive confidence and adaptive curiosity. Technical report, Institut fur Informatik, Technische Universität München, Arcisstr. 21, 800 Munich 2, 1991.

[38] J. Schulman, F. Wolski, P. Dhariwal, A. Radford, and O. Klimov. Proximal policy optimization algorithms. *arXiv preprint arXiv:1707.06347*, 2017.

[39] M. Shridhar, J. Thomason, D. Gordon, Y. Bisk, W. Han, R. Mottaghi, L. Zettlemoyer, and D. Fox. Alfred: A benchmark for interpreting grounded instructions for everyday tasks. In *Computer Vision and Pattern Recognition (CVPR)*, 2020.

[40] M. Stolle and D. Precup. Learning options in reinforcement learning. In *Proceedings of the 5th International Symposium on Abstraction, Reformulation and Approximation*, 2002.

[41] R. S. Sutton, D. Precup, and S. Singh. Between MDPs and semi-MDPs: A framework for temporal abstraction in reinforcement learning. *Artificial intelligence*, 112:181–211, 1999.

[42] S. Tellex, T. Kollar, S. Dickerson, M. R. Walter, A. G. Banerjee, S. J. Teller, and N. Roy. Understanding natural language commands for robotic navigation and mobile manipulation. In *Association for the Advancement of Artificial Intelligence (AAAI)*, 2011.

[43] J. Thomason, S. Zhang, R. J. Mooney, and P. Stone. Learning to interpret natural language commands through human-robot dialog. In *International Joint Conference on Artificial Intelligence (IJCAI)*, 2015.

[44] S. I. Wang, S. Ginn, P. Liang, and C. D. Manning. Naturalizing a programming language via interactive learning. In *Association for Computational Linguistics (ACL)*, 2017.

[45] X. E. Wang, Q. Huang, A. Celikyilmaz, J. Gao, D. Shen, Y.-F. Wang, W. Y. Wang, and L. Zhang. Reinforced cross-modal matching and self-supervised imitation learning for vision-language navigation. In *Computer Vision and Pattern Recognition (CVPR)*, 2019.

[46] N. Waytowich, S. L. Barton, V. Lawhern, and G. Warnell. A narration-based reward shaping approach using grounded natural language commands. In *International Conference on Machine Learning (ICML)*, 2019.

[47] H. Yu, H. Zhang, and W. Xu. A deep compositional framework for human-like language acquisition in virtual environment. *arXiv preprint arXiv:1703.09831*, 2017.
A Experiment Details

Table 2 provides additional reference information about our suite of evaluation tasks.

Table 2: Details of our low- and high-level tasks.

| Low-Level Task       | # Instr. | Example                  | Visualization |
|----------------------|----------|--------------------------|---------------|
| GoTo-Room (G1)       | 36       | *go to a yellow ball*    |               |
| GoTo-Maze (G2)       | 42       | *go to a red key*        |               |
| Open-Maze (O2)       | 6        | *open the green door*    |               |
| Pick-Maze (P2)       | 36       | *pick up a red box*      |               |

| High-Level Task       | # Instr. | Example                                      | Visualization   | $G_i$ |
|-----------------------|----------|----------------------------------------------|-----------------|-------|
| PutNext-Room          | 306      | *put the blue key next to the yellow ball*  |                 | G1    |
| PutNext-Maze          | 1440     | *put the yellow ball next to a purple key*  |                 | G2    |
| Unlock-Maze           | 6        | *open the green door*                       |                 | P2    |
| Open&Pick-Maze        | 216      | *open the yellow door and pick up the grey ball* |               | O2, G2 |
| Combo-Maze            | 1266     | *pick up the green ball*                    |                 | G2    |
| Sequence-Maze         | $\geq$1M| *open the grey door after you put the yellow ball next to a purple key* |               | G2    |
Figure 5: The actor-critic architecture processes an observation and language instruction using a multimodal encoder based on feature-wise linear modulation (FiLM) [34]. It then uses an LSTM to recurrently process a history of observations and projects the output onto actor and critic heads.

Figure 6: The relevance classifier consists of a Siamese network that returns a binary prediction of whether a low-level instruction is relevant to a high-level instruction.

B Training Details

We adapt the PPO implementation from [11] with the default hyperparameters (discount factor of 0.99, learning rate (via Adam) of $7 \times 10^{-4}$, batch size of 2560, minibatch size of 1280, entropy coefficient of 0.01, value loss coefficient of 0.5, clipping-$\epsilon$ of 0.2, and generalized advantage estimation parameter of 0.99). We use the actor-critic architecture from [11] (Figure 5).

B.1 Termination and Relevance Classifiers

The termination classifier $h^\phi$ is an adapted version of the architecture in Figure 5 that uses a binary prediction head instead of the actor and critic heads. Our implementation of $h^\phi$ makes predictions based on single observations; in our BabyAI tasks, final observations are sufficient for evaluating whether a task has terminated.

To train $h^\phi$, we require positive and negative examples of states at which low-level language instructions terminate. We use the automated expert built into BabyAI to generate 15K low-level episodes. For each episode, we use the final observation as a positive example for that episode’s language instruction and a randomly sampled state from the trajectory as a negative example. Similarly, we generate 200 episodes for validation data. We augment the datasets with additional negative examples by sampling 35 mismatching low-level instructions for each terminating observation. We use a batch size of 2560 and optimize via Adam with a learning rate of $10^{-4}$. We train for 5 epochs and use the iteration that achieves the highest validation accuracy.

We train the relevance classifier $f^\rho$ online with the architecture described in Figure 6. For an initialization conducive to deduplication, we initialize $f^\rho$ to predict that any $g^\ell$ is relevant to any $g$. To do this, we randomly sample 100 high-level instructions, cross that set with $G^\ell$, label the pairs as relevant, and train for 20 epochs. We use a learning rate of $10^{-4}$ and a batch size of 10. Online updates based on the online dataset $D$ involve 3 gradient updates to $\rho$ for every 50 iterations of PPO.
B.2 LEARN

We will now detail LEARN [17] which we use as a baseline. LEARN rewards trajectories that it predicts are relevant to a given language instruction. We reimplement LEARN based on an open-source implementation.² We collect 15K episodes of BabyAI’s automated expert completing low-level tasks and process them to create (instruction, action frequency) data. We use this dataset to train the classifier used in LEARN which predicts whether the action frequencies of the current trajectory are related to the current instruction. The coefficient on the shaped rewards is a hyperparameter; based on an informed sweep of values, we set its value to 0.01. We train the classifier for 100 epochs.

An intuition for why LEARN has strong performance in static environments as in [18] but not in our setting is that the method requires action frequencies to provide a signal about whether the current trajectory is related to the language instruction. Our environments are dynamic, and so individual actions are less correlated to language tasks. Additionally, in our setting, the instructions during RL are high-level instructions which are selected from a different distribution than the low-level instructions available for training the classifier.

B.3 RIDE

As an additional comparison point to ELLA, we reimplement the RIDE method [35] based on an open-source implementation.³ RIDE rewards “impactful” changes to the state; we discuss the method further in Appendix D. We use the same architectures as the original work for the forward dynamics model, inverse dynamics model, and state embedding model. For comparability with our implementation of ELLA with PPO, we adapt RIDE to the on-policy setting by updating the dynamics models once per batch of on-policy rollouts. For hyperparameters, we use the values published in the code repository for the coefficients on forward dynamics loss and inverse dynamics loss (10 and 0.1 respectively), as well as the published value for learning rate of 10⁻⁴. We tune the intrinsic reward coefficient (which we call \( \lambda_R \)) within the set \{0.1, 0.5, 1\}.

C Algorithm (Expanded)

Algorithm 2 breaks down ELLA in detail.

²https://github.com/prasoongoyal/rl-learn
³https://github.com/facebookresearch/impact-driven-exploration
Algorithm 2 Reward Shaping with ELLA

1: **Input:** Initial policy parameters $\theta_0$, relevance classifier parameters $\rho_0$, update rate $\eta$, low-level bonus $\lambda$, and on-policy RL optimizer $\text{OPTIMIZE}$
2: Initialize $D \leftarrow \{(g : \mathcal{G}_\ell) \text{ for all } g \in \mathcal{G}\}$
3: for $k = 0, 1, \ldots$ do
4: Collect trajectories $D_k = \{\tau_i\}$ using $\pi^{\theta_k}$.
5: for $\tau \in D_k$ do
6: Set $N \leftarrow$ length of $\tau$
7: Set $(r'_{1:N}, \hat{S}) \leftarrow \text{SHAPE}(\tau)$  
8: if $U(\tau) > 0$ then  
9: Set $r'_N \leftarrow \text{NEUTRALIZE}(r'_{1:N})$
10: Set $D[g] \leftarrow \text{UPDATEDECOMP}(D, \hat{S})$
11: Update $\theta_{k+1} \leftarrow \text{OPTIMIZE}(r'_{1:N})$.
12: if $k$ is a multiple of $\eta$ then
13: $D' \leftarrow$ Sample positive and negative examples of relevant pairs $(g, g_\ell)$ from $D$
14: Update $\rho_{k+1} \leftarrow$ Optimize cross entropy loss on $D'$
15: 
16: function $\text{SHAPE}(\tau)$
17: Set $\hat{S} \leftarrow \emptyset$
18: for $g_\ell \in \mathcal{G}_\ell$ do
19: for $g, (s_t, r_t) \in \tau$ do
20: if $h^\phi(s_t, g_\ell) = 1$ and $g_\ell \notin \hat{S}$ then  
21: Update $\hat{S} \leftarrow \hat{S} \cup \{g_\ell\}$  
22: if $f^\rho(g_\ell) = 1$ then  
23: Set $r'_t = r_t + \lambda$
24: return $(r'_{1:N}, \hat{S})$
25: 
26: function $\text{NEUTRALIZE}(r'_{1:N})$
27: Set $T_S \leftarrow \{t | 1 \leq t \leq N, r'_t > 0\}$  
28: return $r'_N - \sum_{t \in T_S} r'_t + \lambda$  
29: 
30: function $\text{UPDATEDECOMP}(D, \hat{S})$
31: Set $\hat{S} \leftarrow D[g]$
32: if $\hat{S} \cap \hat{S} = \emptyset$ then
33: return $\hat{S}$
34: else
35: return $\hat{S} \cap \hat{S}$

Figure 7: Learning curves for PPO (no shaping), ELLA, RIDE, and ELLA+RIDE in the SEQUENCE-MAZE task. For PPO, ELLA, and ELLA+RIDE, translucent regions show standard deviation of return over three random seeds.

D Relation to Intrinsic Motivation

As mentioned in Section 2, curiosity and intrinsic motivation methods use reward shaping to incentivize exploration to novel, diverse, or unpredictable parts of the state space [9, 33, 35, 37]. We adapt RIDE [35], an intrinsic motivation method, to our setting and discuss one way in which ELLA could be combined with intrinsic motivation methods.

RIDE rewards actions that produce “impactful” changes to its representation of the state. The state representation function is learned via a forward dynamics model and inverse dynamics model. Intuitively, such a representation contains information only relevant to environment features that the agent can control and features that can have an effect on the agent. RIDE does not consider goal-conditioning, so we do not include language instructions in the observation provided to RIDE.

RIDE’s intrinsic rewards are equal to the L2 norm of the difference in this state representation between time steps, scaled by a coefficient $\lambda_R$. We find that $\lambda_R$ can have a sizeable effect on the performance of RIDE, so we tune this hyperparameter as discussed in Section B.3.

We experiment with RIDE in several of the BabyAI tasks, and examine the SEQUENCE-MAZE task as a case-study below. In Figure 7, we compare RIDE with various values of $\lambda$ to ELLA. The SEQUENCE-MAZE task is extremely sparse, and the language instructions are highly diverse. Both RIDE, which rewards impactful state changes, and ELLA, which rewards completion of low-level tasks, have a positive effect on sample efficiency. We additionally test how ELLA+RIDE can be combined; to do this, we simply sum the shaped rewards via ELLA and RIDE at each time step. For this task, we see that the combination of subtask-based exploration (based on an online-learned model of language abstractions) and impact-based exploration (based on online-learned dynamics models) leads to a further increase in sample efficiency.

While these two methods reward different aspects of exploration, and combining them has the potential to improve upon the individual methods, a limitation of this approach is that we must resort to ad hoc methods for tuning shaped reward weights in the combined version. The discussion in Section 4.3 on selecting ELLA’s $\lambda$ hyperparameter does not apply to reward functions that are non-sparse, which occurs when additional intrinsic rewards are included.

In SEQUENCE-MAZE, tuning $\lambda$ and $\lambda_R$ for ELLA and RIDE in isolation and then adding the shaped rewards was effective, but this does not hold for all of the environments. As a representative example of this case, Figure 7 compares a tuned version of ELLA+RIDE in with $\lambda = 0.1$ and $\lambda_R = 0.05$ for the Unlock-Maze task. Here, summing the methods did not significantly outperform either individual method. We observe similar behavior in the PUTNEXT-ROOM environments. Future work could examine how best to fuse subtask-based exploration with intrinsic motivation, or how to weigh different types of intrinsic rewards.
Figure 8: Learning curves in the OPEN&PIEC-MAZE environment for vanilla PPO and ELLA with different data budgets for the termination classifier.

Figure 9: An ablation of ELLA’s relevance classifier, where it is replaced with an oracle, in comparison to ELLA and PPO (no shaping).

### E Ablations

Our approach has two learned components: the termination classifier $h^\phi$, which we train offline using annotated examples of low-level termination states, and the relevance classifier $f^\rho$, which is trained online during RL. To understand how these two modules impact performance, we perform ablations on the termination classifier (by varying its offline data budget) and the relevance classifier (by replacing the online version with an oracle).

#### E.1 Termination Classifier

One of the assumptions of our method is that examples of low-level termination states are inexpensive to collect. As noted in Section B.1, we train the termination classifier in ELLA with 15K positive and negative examples, such that it achieves 99% accuracy on a balanced validation set. We perform an ablation on the termination classifier by training the termination classifier with lower data budgets, and find that we can reduce the data budget to 2K without affecting ELLA’s performance. However, with a data budget as low as 500, ELLA’s performance declines. With a data budget of 100, the termination classifier has an accuracy of only 66%, and the shaped rewards are noisy enough that the overall learning curve is degenerate.
E.2 Relevance Classifier

The relevance classifier is trained online using the relevance dataset $\mathcal{D}$. As an ablation for this module, we replace the relevance classifier with an oracle. To mimic the way that the relevance classifier is initialized to predict that all low-level tasks are relevant to a high-level instruction, we reward all low-level tasks for the first 2.5 million frames before switching to the oracle predictions. This initial phase incentivizes low-level task completion generally, as ELLA does, and is empirically beneficial.

Figure 9 shows learning curves for PPO (no shaping), ELLA, and ELLA with the oracle relevance classifier. The oracle version slightly outperforms ELLA for three of the four tasks and performs similarly on the SEQUENCE-MAZE task. This task has over $10^6$ instructions and remains challenging even with low-level bonuses.

F Proof of Policy Invariance

In this section, we sketch the proof of the policy invariance of our reward transformation. We begin with the goal-conditioned MDP $\mathcal{M} = (\tilde{S}, \tilde{A}, \tilde{T}, \tilde{R}, \tilde{G}, \gamma)$, where $\tilde{\mathcal{T}}: \tilde{S} \times \tilde{A} \times \tilde{S} \rightarrow [0, 1]$ and $\tilde{\mathcal{R}}: \tilde{S} \times \tilde{A} \times \tilde{S} \times \tilde{G} \rightarrow [0, R_{\text{max}}]$. $\tilde{\mathcal{R}}$ is sparse. Let $\tilde{\mathcal{M}}$ be an augmented MDP $(\tilde{\tilde{S}}, \tilde{\tilde{A}}, \tilde{\tilde{T}}, \tilde{\tilde{R}}, \tilde{\tilde{G}}, \gamma)$ which stores state histories: that is, $\tilde{s}_t = (s_t, h_{0:t-1})$. $\tilde{\mathcal{T}}: \tilde{\tilde{S}} \times \tilde{\tilde{A}} \times \tilde{\tilde{S}} \rightarrow [0, 1]$ is defined as $T_t(\tilde{s}_t, a_t, \tilde{s}_{t+1}) = T(s_t, a_t, s_{t+1}) \cdot h_{0:t} = (h_{0:t-1}, s_t)$. $\tilde{\mathcal{R}}$ is defined similarly to reflect consistency between histories. The transformation from $\mathcal{M}$ to $\tilde{\mathcal{M}}$ does not affect optimal policies because we are simply appending history information to the state without affecting the dynamics. We now use $\tilde{\mathcal{M}}$ (instead of $\mathcal{M}$) to show policy invariance with a given shaped MDP $\mathcal{M}'$, as we describe below.

Consider a shaped MDP $\mathcal{M}' = (\tilde{\tilde{S}}, \tilde{\tilde{A}}, \tilde{\tilde{T}}', \tilde{\tilde{R}}, \tilde{\tilde{G}}, \gamma)$ where $\tilde{\tilde{T}}': \tilde{\tilde{S}} \times \tilde{\tilde{S}} \rightarrow [0, 1]$ is defined as $\tilde{\tilde{T}}'(\tilde{s}_t, a_t, \tilde{s}_{t+1}) = \tilde{\tilde{T}}(\tilde{s}_t, a_t, \tilde{s}_{t+1}) + \ell(\tilde{s}_t, \tilde{s}_{t+1})$ where $\ell: \tilde{\tilde{S}} \rightarrow \mathbb{R}$ represents the low-level task bonuses (or neutralization penalty) going from state $\tilde{s}_t$ to $\tilde{s}_{t+1}$ as defined in Section 4.3. We first aim to show that the transformation from $\mathcal{M}$ to $\mathcal{M}'$ does not introduce new optimal policies—that is, any optimal policy in $\mathcal{M}'$ is also optimal in $\tilde{\mathcal{M}}$.

Let $\tilde{\pi}_{\tilde{\mathcal{M}}}(\tilde{s}) = \pi_{\mathcal{M}'}(\tilde{s})$ where $\pi_{\mathcal{M}'}$ is optimal in $\mathcal{M}'$. We will show this policy is also optimal in $\tilde{\mathcal{M}}$: that is, $V_{\pi_{\tilde{\mathcal{M}}}} = V^*_{\tilde{\mathcal{M}}}(\tilde{s}_t)$ for all $\tilde{s}_t$. Since $\tilde{\mathcal{R}}$ is nonnegative and sparse, we only need to consider states $\tilde{s}_t$ at which the value could possibly be positive: those from which the task is solvable in at most $H - t$ steps, where $H$ is the horizon.

Assume the task is solvable in a minimum of $k \leq H - t$ steps (using an optimal policy in $\tilde{\mathcal{M}}$). We can reason about $\tilde{\pi}_{\tilde{\mathcal{M}}}(\tilde{s}) = \pi_{\mathcal{M}'}(\tilde{s})$ by considering the various ways return could be accumulated in $\mathcal{M}'$, and of those cases yields the maximum return.

(1) A policy could solve the task in $j \geq k$ steps while solving subtasks at timesteps $T_\delta$, and receive a discounted future return of $\sum_{t' \in T_\delta \cap t' \geq t} \gamma^{t'-t} \lambda + \gamma^j (R_{\text{max}} - \sum_{t' \in T_\delta \cap t' < t} \gamma^{t'-t} \lambda)$.

(2) A policy could solve only subtasks at timesteps $T_\delta$ and receive a discounted future return of $\sum_{t' \in T_\delta \cap t' \geq t} \gamma^{t'-t} \lambda$.

We can simplify the return in case (1) to $\gamma^j R_{\text{max}} - \sum_{t' \in T_\delta \cap t' < t} \gamma^{t'-t} \lambda$. The second term does not depend on actions taken after $t$; thus, this case is maximized by completing the task in $j = k$ steps.

Note that case (2) always gets smaller return than case (1): the first term, $\sum_{t' \in T_\delta \cap t' \geq t} \gamma^{t'-t} \lambda$, is the same as in case (1), and the second term in case (1) is strictly positive when we use the bound on $\lambda$ from Section 4.3: that $\lambda < \frac{\gamma^HR_{\text{max}}}{1-\gamma}$. Therefore, the maximum future return is achieved in case (1), specifically by a policy that solves the task in $k$ steps, and we know that this policy exists. Thus $V_{\pi_{\tilde{\mathcal{M}}}}(\tilde{s}_t) = \gamma^k R_{\text{max}} = V^*_{\tilde{\mathcal{M}}}(\tilde{s}_t)$, and so an optimal policy in $\mathcal{M}'$ is also optimal in $\tilde{\mathcal{M}}$. In order to show the reverse, we can use similar logic to show that any optimal policy in $\tilde{\mathcal{M}}$ acts optimally in $\mathcal{M}'$ for any state $\tilde{s}_t$ where the task is solvable in a minimum of $k \leq H - t$ steps; actions towards solving the task most quickly are also optimal in $\mathcal{M}'$. Together, this shows policy invariance between $\mathcal{M}$ and $\mathcal{M}'$ for the set of states $\tilde{s}_t$ where the task is solvable.