A PATCHY CLOUD MODEL FOR THE L TO T DWARF TRANSITION

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ABSTRACT

One mechanism suggested for the L to T dwarf spectral type transition is the appearance of relatively cloud-free regions across the disk of brown dwarfs as they cool. The existence of partly cloudy regions has been supported by evidence for variability in dwarfs in the late L to early T spectral range, but no self-consistent atmosphere models of such partly cloudy objects have yet been constructed. Here, we present a new approach for consistently modeling partly cloudy brown dwarfs and giant planets. We find that even a small fraction of cloud holes dramatically alter the atmospheric thermal profile, spectra, and photometric colors of a given object. With decreasing cloudiness objects briskly become bluer in \( J - K \) and brighten in \( J \) band, as is observed at the L/T transition. Model spectra of partly cloudy objects are similar to our models with globally homogenous, but thinner, clouds. Hence, spectra alone may not be sufficient to distinguish partial cloudiness although variability and polarization measurements are potential observational signatures. Finally, we note that partial cloud cover may be an alternative explanation for the blue L dwarfs.

Key words: brown dwarfs – stars: atmospheres

Online-only material: color figures

1. INTRODUCTION

As brown dwarfs cool over time, their atmospheres undergo a sequence of chemical and physical changes that result in an evolving emergent spectrum and—consequently—varying spectral types. The most remarkable changes take place at the L to T type transition. The latest L dwarfs have red near-infrared colors, strong CO absorption in \( K \) band and relatively shallow water absorption bands modulating their spectra. Over a small effective temperature range of only 100–200 K the spectrum rapidly changes to exhibit blue near-infrared color, weakening CO absorption, strengthening CH4 absorption, and deeper water bands (see Kirkpatrick 2005 for a review).

The proximal cause of these changes is the loss of cloud opacity. As clouds dissipate the visible atmosphere cools, bringing on the chemical change from CH4 to CO. Without clouds providing a significant, nearly gray opacity, flux can emerge through molecular opacity windows in the \( J \) and \( H \) bands with a brightening leading to a blueward color shift (Dahn et al. 2002; Tinney et al. 2003; Vrba et al. 2004). Studies of L+T binary dwarfs (e.g., Liu et al. 2006; Looper et al. 2008; Stumpf et al. 2010 and references therein) show that this brightening is an intrinsic signature of the transition and not the manifestation of some other effect in color–magnitude diagrams (Stumpf et al. 2010). Two main underlying causes of this loss in cloud opacity have been suggested. In one view the atmospheric dynamical state changes, resulting in larger particle sizes that more rapidly “rain out” of the atmosphere, leading to a sudden clearing or collapse of the cloud (Knapp et al. 2004; Tsuji & Nakajima 2003; Tsuji et al. 2004). This view is supported by fits of spectra to model spectra (Saumon & Marley 2008) computed with the Ackerman & Marley (2001) cloud model. In that formalism a tunable parameter, \( f_{\text{sed}} \), controls cloud particle sizes and optical depth. Larger \( f_{\text{sed}} \) yields larger particles along with physically and optically thinner clouds. Cushing et al. (2008) and Stephens et al. (2009) have demonstrated that progressively later T dwarfs can be fit by increasing \( f_{\text{sed}} \) across the transition. Late T dwarfs are generally best fit by models that neglect cloud opacity. Burrows et al. (2006) also suggest changes in cloud particle sizes as a possible mechanism.

The second view is inspired by thermal infrared images of the atmospheres of Jupiter and Saturn at \( \sim 5 \mu \text{m} \) (e.g., Westphal 1969; Westphal et al. 1974; Orton et al. 1996; Baines et al. 2005). In this spectral region, gaseous opacity is very low, allowing flux from deeply seated, warm atmospheric regions to escape. Higher lying clouds, however, locally reduce the emergent flux. As a result, these planets take on a mottled appearance with bright high-flux, low cloud opacity regions lying adjacent to cooler, darker, and cloudier regions (optical depth varies from \( \sim 0 \) to \( \sim 20 \) between these regions Banfield et al. 1998). Ackerman & Marley (2001) suggested that the arrival of such cloud holes near the end of the L spectral sequence may be responsible for the L to T transition. Burgasser et al. (2002) tested this hypothesis with a simple “toy model” by summing weighted contributions of the spectra of cloudy and cloudless models. They showed that the observed \( J \)-band brightening across the transition could arise from decreasing cloud coverage. Further support for this hypothesis comes from observations of L and T dwarf variability. While previous studies were somewhat equivocal (summarized in Artigau et al. 2009), two early T dwarfs have recently been shown to have large near-infrared photometric variability (Artigau et al. 2009; J. Radigan et al. 2010, in preparation) consistent with surface variations in cloud coverage modulated by rotation.

The approach to modeling holes of Burgasser et al. was highly simplistic. The principal shortcoming being that it is not physically correct to combine the contributions of separate cloudy and cloudless models. Deep in the atmosphere of a brown dwarf the entropy in the convection zone must match that of the interior. Thus, the temperature at a given, deep pressure level is expected to be horizontally constant. However for a fixed \( T_{\text{eff}} \) a cloudy atmosphere is everywhere hotter than a cloudless atmosphere. As an example, Figure 1 presents model atmosphere profiles for a uniform cloudy and a cloudless
atmosphere following the techniques of Marley et al. (2002) and Saumon & Marley (2008). At depth, the cloudy profile is warmer than the cloudless profile by over 400 K; the difference in some models is even greater. Thus, standard cloudy and cloudless models cannot simultaneously be valid descriptions of the real atmosphere at two locations even though both models are descriptions of an atmosphere with the same $T_{\text{eff}}$. Clearly a new technique for self-consistently treating partly cloudy atmospheres is required. While we do not yet understand why cloud holes might appear, we here present a new approach inspired from models of Earth’s atmosphere to model their influence and apply our results to model the spectra and colors of L and T dwarfs.

2. MODELING PARTLY CLOUDY SKIES

Instead of combining separately computed profiles for purely cloudy and cloud-free dwarfs, we wish to construct a single, global temperature–pressure profile $T(P)$ that simultaneously incorporates the influences of both cloudy and cloud-free regions on the energy balance of the atmosphere. The final profile should conserve the total flux while allowing for nearby atmospheric regions to have differing cloud—but not thermal—profiles. This conceptually allows clouds to be displaced by winds, updrafts, or downdrafts, and change location, as long as the global mean cloud fraction is constant.

In three-dimensional terrestrial numerical weather prediction models, clouds are typically smaller than the adopted computational grid scale. Various methods are used to treat this in the radiative transfer calculations, one of which is to consider separate cloudy and cloud-free sub-columns in the same model column, with a single $T(P)$ structure. This same approach can be used in a single column model of the Earth, allowing the global annual mean energy budget to be reproduced (Goldblatt & Zahnle 2010).

Physically, such considerations are most important on Earth in the tropics. Taking the zonal mean $T(P)$ and moisture profile would give a local runaway greenhouse due to the high water vapor content. However, dry areas in the tropics caused by subsiding air act as “radiator fins,” allowing radiation from the surface to escape to space (Pierrehumbert 1995). In brown dwarfs atmospheres, cloud-free areas would be analogous to the subsidence regions in Earth’s tropics.

To implement this approach, we set the parameter $0 \leq h \leq 1$ to be the fraction of the atmosphere described by the cloud-free sub-column, from which the local flux at some level in the atmosphere is $F_{\text{hole}}$. The remaining fraction $(1 - h)$ is the cloudy sub-column, with local flux $F_{\text{cloud}}$. Both sub-columns share the same $T(P(z))$ profile but have different emergent flux, in general $F_{\text{hole}} > F_{\text{cloud}}$. We compute the total flux, $F_{\text{tot}}(z)$, through the atmosphere, which is used in the radiative–convective equilibrium calculation, as

$$F_{\text{tot}}(z) = h F_{\text{hole}}(z) + (1 - h) F_{\text{cloud}}(z).$$

We stress that this is not a combination of separate models, but rather conceptually represents two adjacent sub-columns in the atmosphere with the same thermal profile and differing opacity. Our radiative–convective equilibrium model is then employed to solve for a single $T(P)$ atmospheric thermal profile (McKay et al. 1989; Marley & McKay 1999) that carries the same $T_{\text{eff}}, h$, and solar metallicity. Solid lines are for atmospheres with horizontally homogenous cloud cover (labeled $f_{\text{sed}} = 2$ and 4) or no clouds (labeled nc). Two partly cloudy models with hole fraction $h = 0.25$ and 0.5 and based on a $f_{\text{sed}} = 2$ cloud model are shown with dashed lines. The condensation curves of iron and forsterite are shown with dotted lines. (A color version of this figure is available in the online journal.)

![Figure 1. Model atmosphere temperature–pressure profiles with $T_{\text{eff}} = 1400$ K, log $g$(cm s$^{-2}$) = 5 and solar metallicity. Solid lines are for atmospheres with horizontally homogenous cloud cover (labeled $f_{\text{sed}} = 2$ and 4) or no clouds (labeled nc). Two partly cloudy models with hole fraction $h = 0.25$ and 0.5 and based on a $f_{\text{sed}} = 2$ cloud model are shown with dashed lines. The condensation curves of iron and forsterite are shown with dotted lines. (A color version of this figure is available in the online journal.)](image)

3. PHOTOMETRY AND SPECTRA OF PARTLY CLOUDY DWARFS

The synthetic spectrum for a converged $T(P)$ atmospheric profile is obtained from Equation (1). We compute absolute magnitudes and colors with the ultracool dwarf evolution models of Saumon & Marley (2008). Figure 2 shows synthetic near-infrared photometry from the partly cloudy models. For a fixed $T_{\text{eff}}$, as $h$ is increased the model colors briskly move to the blue in $J - K$ and $J - H$. The J-band flux increases as $h$ increases from 0 to 0.75, but then dims slightly for cloud-free models.
partly cloudy model colors with partly cloudy model colors with $f_{\text{sed}} = 2$ and cloudless models (both $\log g = 5$). Horizontal green lines connect partly cloudy model colors with $T_{\text{eff}} = 1000-2000$ K in steps of 200 K (from bottom to top). Partly cloudy models (green dots) are for cloud-free fractions $h$ of 0, 0.25, 0.5, 0.75, and 1, from right to left. Square symbols show field dwarfs with M dwarfs in black, L dwarfs in red, and T dwarfs in blue. The photometry is of 0, 0.25, 0.5, 0.75, and 1, from right to left. Square symbols show field dwarfs with M dwarfs in black, L dwarfs in red, and T dwarfs in blue. The photometry is primarily from Leggett et al. (2002) and Knapp et al. (2004). Additional sources are given in Saumon & Marley (2008, Figure 7).

\begin{figure}[h]
\centering
\includegraphics[width=0.8\textwidth]{figure2.pdf}
\caption{Near-infrared model color–magnitude diagrams (MKO system). Red and blue lines, respectively, show model colors for cloudy sequence with $f_{\text{sed}} = 2$ and cloudless models (both $\log g = 5$). Horizontal green lines connect partly cloudy model colors with $T_{\text{eff}} = 1000-2000$ K in steps of 200 K (from bottom to top). Partly cloudy models (green dots) are for cloud-free fractions $h$ of 0, 0.25, 0.5, 0.75, and 1, from right to left. Square symbols show field dwarfs with M dwarfs in black, L dwarfs in red, and T dwarfs in blue. The photometry is primarily from Leggett et al. (2002) and Knapp et al. (2004). Additional sources are given in Saumon & Marley (2008, Figure 7).}
\end{figure}

$h = 1$). This is because atmospheres with even a small cloud cover are warmer in the atmospheric region from which the $J$-band flux emerges. On the other hand, $M_H$ is relatively constant across the transition from $h = 0$ to $h = 1$ at constant $T_{\text{eff}}$ but shows a similar dimming as $h \rightarrow 1$.

The evolution of model dwarfs with fixed $f_{\text{sed}}$ produces trajectories that do not exhibit a rapid L to T transition as a global homogenous cloud sinks too gradually below the photosphere (Burrows et al. 2006; Saumon & Marley 2008, Figure 4). With the Ackerman & Marley (2001) cloud model, the L to T dwarf transition can only be modeled with an increase of the cloud sedimentation parameter $f_{\text{sed}}$. Figure 2 demonstrates that the transition can also be described as a progressive increase in cloud-free areas at a fixed $f_{\text{sed}}$ and $T_{\text{eff}} \sim 1200$ K. The L/T transition dwarf colors and the $J$-band brightening are well fit by this approach. However, 1200 K is slightly cooler than the observed $T_{\text{eff}}$ temperature of the transition of $\sim 1300$ K (Golimowski et al. 2004; Stephens et al. 2009) and if $T_{\text{eff}}$ falls appreciably across the transition the $J$-band bump would be weakened (Figure 2). For a different choice of $f_{\text{sed}}$ and model gravity a different $T_{\text{eff}}$ would be expected.

As noted in Saumon & Marley (2008), there is an offset of $\sim 0.3$ to the blue in the $J - K$ color of models from the bulk of L and T dwarf photometry. This may arise from shortcomings in the $K$-band pressure-induced opacity of molecular hydrogen. Nonetheless, the trend of the late T dwarf $J - K$ color can be better reproduced with models with $h \sim 0.5-0.75$. In the $M_H$ versus $J - H$ diagram, the behavior of field L dwarfs and late T dwarfs are better reproduced by the cloudy $f_{\text{sed}} = 2$ and the cloudless sequences, respectively, although the latter would also be better matched with partly cloudy models with $h \sim 0.5-0.75$. This suggests the spectra of late T dwarfs could be influenced by clouds, contrary to the usual assumption (Burgasser et al. 2010).

4. DISTINGUISHING PARTLY CLOUDY DWARFS

In Saumon & Marley (2008), we demonstrated that by increasing the cloud sedimentation efficiency $f_{\text{sed}}$ as a brown dwarf cools from $T_{\text{eff}} = 1400$ to 1200 K, the predicted model colors reproduce those across the L to T transition. In the previous section, we likewise showed that increasing fractional cloudiness—at fixed $f_{\text{sed}}$—has the same result. This leads us to consider how to distinguish the two cases.

As shown in Figure 1 a partly cloudy $T(P)$ profile (based on a $f_{\text{sed}} = 2$ cloud) can be nearly identical to a model with a thinner homogenous cloud but the spectrum from these two models is not necessarily the same because the former uses Equation (1) to compute the flux. In the partly cloudy case some flux from deep, hot regions of the atmosphere ($r_{\text{hole}}$) is escaping through the clear regions that are otherwise totally shielded by the cloud in the homogeneous case (see the middle panel of Figure 7 of Ackerman & Marley 2001). Thus, we expect that even for identical $T(P)$ profiles the emission spectra will differ.

Indeed that is the case as shown in Figure 3 which shows spectra computed from profiles shown in Figure 1. Focusing on the $J$ band, which features the lowest molecular opacity and the deepest atmospheric window in the near-infrared (Ackerman & Marley 2001), the greatest flux is found for the cloudless model. The homogenous cloudy $f_{\text{sed}} = 2$ model is faintest, with the $f_{\text{sed}} = 4$ case falling in between. Even though the partly cloudy $h = 0.5$ model has essentially the same thermal profile as the $f_{\text{sed}} = 4$ model, it is brighter in the $J$ band because some flux is escaping from deeper in the atmosphere. Of course flux conservation requires that the partly cloudy model must be fainter at other wavelengths, here in the $K$ band. Thus, the model spectra are increasingly bluer in the near-infrared from $f_{\text{sed}} = 2$
to $f_{\text{sed}} = 4$ to the partly cloudy model. Figure 3 shows that the partly cloudy model is very close to the $f_{\text{sed}} = 4$ homogeneous cloudy model at wavelengths where the flux is low and emitted from the upper atmosphere, and intermediate between $f_{\text{sed}} = 4$ and cloudless in the $JHK$ flux peaks where part of the flux comes from the deeper atmosphere. Thus, for a given $T_{\text{eff}}$ and gravity, the presence of holes in the cloud cover has a discernible effect on the near-infrared spectrum.

For a given observed spectrum, where $T_{\text{eff}}$, gravity, and composition are not known a priori, how can we distinguish a partly from a homogeneous cloudy atmosphere? We explored this problem by fitting the near-infrared partly cloudy model spectra with our large library of cloudy models, using the method of Cushing et al. (2008), and allowing $T_{\text{eff}}$, gravity, and $f_{\text{sed}}$ to vary freely. We find that in general, the best-fitting cloudy model has the same gravity, the same $T_{\text{eff}}$ (or slightly higher by $\sim 100$ K) and a higher $f_{\text{sed}}$ depending on $h$. The fitted cloudy spectra are close to the partly cloudy spectra, and some of the differences can be attributed to the grid spacing of the cloudy models. It appears that the $JHK$ colors of a partly cloudy model ($T_{\text{eff}}$, $g$, $f_{\text{sed}}$, $h$) can be well matched with a cloudy model ($T'_{\text{eff}}$, $g'$, $f'_{\text{sed}}$, $h'$). The differences in the near-infrared spectrum are thus subtle and comparable to the differences found between observed spectra and the best-fitting models (e.g., Cushing et al. 2008; Stephens et al. 2009). Given that even with bolometric luminosity measurements $T_{\text{eff}}$ temperatures cannot yet be measured to much better than $\sim 50$ K precision, effective temperature cannot yet provide a strong constraint on $h$. The most promising avenue to distinguish the two models in the L/$T$ transition spectrosopically appears to be strong spectral features that are very sensitive to temperature and that are formed in the deeper, hotter regions of the atmospheres, such as the $0.99 \mu$m band of FeH and the alkali doublets of Na I (1.14 $\mu$m) and K I (1.175 and 1.25 $\mu$m). Those should become stronger as the cloud coverage decreases.

Given these considerations, variability may be the best method of characterizing cloud patchiness in brown dwarfs. Partly cloudy dwarfs may be variable if the lengthscales of the cloudy patches are large enough and if the viewing inclination is not near pole on. Variations in the geometry of the cloud cover (“weather”) would also lead to detectable variations in brightness on time scales different from the rotation period. Indeed there is indication that a sizable fraction of L dwarfs are variable (Gelino et al. 2002; Koen 2003). Sample sizes are as yet too small to determine if blue L dwarfs or L/$T$ transition objects show greater variability than other L dwarfs, but systematic studies would elucidate any trends.

Polarization is another possible way to distinguish partly from fully cloudy objects. Cloud-free brown dwarfs should not show appreciable polarization (Sengupta & Marley 2009). Sengupta & Marley (2010) demonstrated that very rapidly rotating, low gravity dwarfs with homogenous clouds can show sizeable polarization, but only for rotation periods less than about 4 hr. However, partly cloudy L dwarfs may show a polarization signal at $I$ band consistent with that observed in some objects (Menard & Delfosse 2004). Measurable polarization in a slowly rotating or high gravity brown dwarf would point to the presence of inhomogeneous cloud cover.

5. DISCUSSION AND CONCLUSIONS

There is growing evidence that the transition from the L to the T spectral class happens over a small effective temperature range (e.g., Stephens et al. 2009). It is difficult for any model of a globally uniform, homogenous cloud to either sink out of sight or precipitate rapidly enough to account for the observed rapid change in spectral properties. Instead the transition may arise as holes appear in an otherwise uniform global cloud deck.

We have presented the first self-consistent method for computing one-dimensional global atmospheric profiles appropriate to an atmosphere which has both clear and cloudy patches. The model does not depend upon the physical sizes of the patches, nor does it explain why patches might appear, but rather parameterizes the global fraction of clear and cloudy regions. The resulting $T(P)$ profiles converged to our model are intermediate in temperature between hot, cloudy models and colder, cloudless ones. We confirm the conclusion of Burgasser et al. (2002), who used a more simplistic model to argue that patchiness in brown dwarf clouds is a plausible mechanism for the L to T type transition.

In addition to the L to T transition, patchy clouds have been suggested by Folkes et al. (2007) as a possible mechanism to explain those L dwarfs that have unusually blue near-infrared colors (Cruz et al. 2003; Knapp et al. 2004; Burgasser et al. 2008). Burgasser et al. (2008) demonstrated that a $T_{\text{eff}} = 1700$ K model with thin ($f_{\text{sed}} = 4$) clouds provides a good spectral match to the blue L dwarf 2MASS J1126–5003. We find that in this effective temperature regime a model with thicker ($f_{\text{sed}} = 2$) and 50% cloud coverage produces a comparable spectrum. Thus, we agree with Folkes et al. (2007) that partial cloudiness is potential alternative mechanism to thin global clouds for the blue L dwarfs. Differences in cloud coverage might result from different rotational rates, gravities, or even viewing geometries (pole versus equator).

The growing evidence for temporal photometric variability at the L to T transition (Artigau et al. 2009; J. Radigan et al. 2010, in preparation) supports the plausibility of partial cloudiness being responsible for the change in colors across the transition. Future three-dimensional simulations of brown dwarf atmospheres (e.g., Freytag et al. 2010) coupled with a new generation of cloud models will likely help to elucidate the underlying mechanism responsible for cloud fragmentation at $T_{\text{eff}} \sim 1200–1300$ K. In the meantime additional observations of brown dwarf photometric variability and observations of L/T binaries will shed light on this poorly understood phase of their evolution.

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