Reduction Kinetics of Fine Hematite Ore Particles in Suspension

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Suspension reduction kinetics of hematite ore particles at 1710 K to 1785 K was described by the Johnson-Mehl-Avrami-Kolmogorov model with Avrami exponent of 1.405. The apparent activation energy is 105.5 kJ mol\(^{-1}\) with the rate determining step of nucleation and growth. The reduction degree of the hematite at the endpoint is a linear function of temperature and the logarithmic oxygen potential of the reacting gas. A peak function of reaction rate constant with particle size has been verified in this work, and the maximum value of the reaction rate is located at around 85 \(\mu\)m particle size. The influence of heat transfer on the reaction process has been evaluated. The results suggest that the heating-up process for large particles, 244 \(\mu\)m particles, for instance, cannot be ignored. It can retard the reaction rate compared to small particles. Normally, the reaction rate constant decreases linearly with the increase of \(\ln[p(O_2)]\) of the reacting gas mixture. However, 95 vol pct CO\(_2\) in the reacting gas can accelerate the reaction rate of thermal decomposition of hematite due to the emissivity of CO\(_2\) gas. It results in a higher reaction rate of 110 \(\mu\)m particles in 95 vol pct CO\(_2\)-containing gas than that in other less CO\(_2\)-containing gases.

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I. INTRODUCTION

Hisarna is an emerging and promising alternative ironmaking process, developed to reduce CO\(_2\) emissions. A smelting cyclone is used to melt and pre-reduce fine and un-agglomerated iron ore particles in the Hisarna reactor. Fine ore and flux are injected in the smelting cyclone together with oxygen. The injected ore is intensely mixed with rising hot reducing gases which undergoes partial reduction and melting. The melt hits the water-cooled sidewalls of the cyclone section and flows down along the wall and into the liquid bath in the smelting reduction vessel (SRV) where the final reduction takes place. The ore in the cyclone section is pre-reduced to a degree of about 20 pct through thermal decomposition and reduction by the SRV gas. The temperature of the melt is approximately 1723 K. There are limited publications about the details of the reaction mechanism and kinetics and are the subject of the present research with High-temperature Drop Tube Furnace (HDTF).

In order to develop alternative ironmaking processes, experimental work has been done to explore the reduction kinetics of iron ore particles in suspension reduction in recent 10 years [1-9]. Especially, the reduction of fine hematite particles has been studied at the temperature range from 1550 K to 1750 K in CO\(_2\) reaching atmospheres to support the development of the Hisarna process [10]. It still needs more experimental work on the high-temperature suspension reduction kinetics, of which the temperature is higher than 1710 K. At such temperature, the reduction products become half molten or fully melted [9]. The effects of reaction temperature, gas composition, and particle size on the reaction kinetics need to be explored. Primarily, the reduction kinetics of ore strongly depend on its nature. Studies of iron ores with different resources and reacting at various conditions are very needed for a comprehensive knowledge of the reduction process.

Experimental work has been done in this work from 1710 K to 1785 K to provide the kinetic information of the reduction process of hematite particles at high temperature. The effect of gas composition, particle size, and temperature on the kinetics are discussed in detail.
II. EXPERIMENTAL

The reduction of hematite particles was carried out in High-temperature Drop Tube Furnace (HDTF) in this study. The raw materials were provided by Tata Steel in IJmuiden. Most of the gangue and hematite phases are distributed in different particles. Therefore, the interaction between the gangue and hematite phases during the reaction can be ignored due to the laminar flow in the reactor.\[11\] The average sizes of the ore particles are 67, 85, 110, 142 and 244 μm. The reaction times are from 72 to 1120 ms. The details of the furnace were described in References 8 and 10. Hematite particles fell through the hot zone in the furnace, reacting with the pre-heated reducing gas, and then were collected in the sealed chamber below the furnace. The reaction temperature range was from 1710 K to 1785 K. The atmosphere is shown in Table I. The ambient pressure is 1 atm.

The mass ratios of total iron (TFe) and Fe\(^{2+}\) of the reacted samples were analyzed with ICP-AES (Inductively Coupled Plasma-Atomic Emission Spectrometry) and chemical titration, respectively. The titration method of Fe\(^{2+}\) follows the ASTM standard test and chemical titration, respectively. The titration method of Fe\(^{2+}\) follows the ASTM standard test method with the designation number of D 3872-05 (2005). The phase composition of the collected samples was detected by semi-quantitative XRD (Bruker D8 Advance X-Ray Diffraction) analysis. The data from ICP-AES and titration are used for kinetic modeling. Non-linear curve fitting module in OriginPro 2015 and 1stOpt 7.0 (authorized to University of Science and Technology Beijing) were combined for kinetic modeling. Levenberg Marquardt method was adopted as the iteration algorithm in the modeling work.

III. RESULTS AND DISCUSSION

A. Reduction Degree

The reduction degree \(R\) of hematite ore is defined as the ratio of mass loss of oxygen to the total initial mass of oxygen in Fe\(_2\)O\(_3\) in the ore. It was employed in this work to calculate the value of \(R\) from the experimental data of titration and ICP-AES measurement:

\[
R = \frac{1}{3} \frac{\text{Fe}^{2+} (\text{mass pct})}{\text{TFe} (\text{mass pct})}
\]

Equation [1] is specifically applied for the reduction of Fe\(_2\)O\(_3\) up to FeO. Here, FeO is the very final product which can be produce with the assigned experimental conditions in this work. For hematite, \(R = 0\) pct, for magnetite \(R = 11\) pct and for wustite \(R = 33.3\) pct. The value of \(R\) can also be obtained from the phase composition:

\[
R = \frac{\text{Fe}_2\text{O}_3 (\text{mass pct})}{48} + \frac{1}{100} \left[ \frac{\text{Fe}_3\text{O}_4 (\text{mass pct}) + 2\, \text{FeO} (\text{mass pct}) + \text{Fe}_2\text{O}_3 (\text{mass pct}) - 100}{\text{Fe}_2\text{O}_3 (\text{mass pct}) + 4\, \text{FeO} (\text{mass pct}) + 2\, \text{Fe}_2\text{O}_3 (\text{mass pct})} \right]
\]

Phase composition is estimated from the XRD results. The depth of X-ray detection is from 2 to 20 μm, so that the information in the core of the particles could be missed in the XRD pattern. Therefore, as Figure 1 shows, the reduction degree calculated from XRD is gradually higher than the value from chemical analysis with increasing value of \(R\). It implies that the reduction is a topochemical reaction.

The most common kinetic analysis contains two steps: (1) To get the values of rate constants \((k)\) from each batch of data independently; (2) To get activation energy from the fitting of \(k–T\) relationship with Arrhenius equation. The fitting results from the first step were usually reported in the literatures as parts of the final kinetic analysis results, although, strictly speaking, they could not be. In order to obtain reliable results, a global fitting method was adopted in the modeling for the whole 23 batches of experiments. The fitting results could not be the best one for a specific batch of experiment data, but it is the optimized result for the whole. In the fitting process, the reaction rate constant was defined as:

\[
k = A \exp \left( \frac{-\Delta E}{R_g T} \right),
\]

where \(A\) is the pre-exponential factor in s\(^{-1}\), \(\Delta E\) is the apparent activation energy in J mol\(^{-1}\), \(R_g\) is gas constant and \(T\) is the temperature in K. The relationship between the reaction rate constant and particle size has been suggested to be a peak function.\[10\] It means that the reaction rate constant of large particles could be higher than the small particles in this specific case. Moreover, the reaction rate constant was suggested to be an inverse relationship with particle size when the particle diameter is larger than 85 μm, for the particular iron ore tested in this study. This trend will be verified in the present work with more experiments at different temperatures. Additionally, the relationship between reaction rate constant and the atmosphere will be discussed.

Our previous study proposed that the reaction rate controlling step of this reduction process is nucleation and growth.\[3\] Johnson–Mehl–Avrami–Kolmogorov model (JMMAK model) is suggested to be employed to describe the reduction process of the particle\[12–14\]:

\[-\ln(1 - z) = (kt)^n,\]

where \(z\) is the reaction fraction, \(k\) is the reaction rate constant, and \(t\) is the residence time, \(n\) is the Avrami exponent.

Equation [4] is employed to simulate the reduction kinetics of hematite particles, where the reaction fraction can be defined as the ratio of reduction degree to the reduction degree at the end of the reaction, \(R_{\text{max}}\):

\[
z = \frac{R}{R_{\text{max}}}
\]

A statistical analysis shows that \(R_{\text{max}}\) is the function of reaction temperature and oxygen potential of the gas system (Figure 2):
\[ R_{\text{max}} = (-165 \pm 25) + (8.62 \pm 1.41) \times 10^{-2} T - (2.16 \pm 0.14) \ln p(O_2), \]

where the oxygen potential of the gas system is extracted from the equilibrium state of the gas mixture, \( p(O_2) \) is oxygen potential in atm. This equation can empirically predict the terminal reduction degree of hematite in the reaction.

For the JMAK model, Avrami exponent, \( n \), is a crucial parameter.\(^{[15–17]}\) Usually, the value of \( n \) is 4 for a three-dimensional nucleation and growth process in an infinite space. Yet, Alekseechkin\(^{[18]}\) pointed out that the Avrami exponent decreases with time from 4 to 1 in homogeneous nucleation and 3 to 0 in specific heterogeneous nucleation in a particle with finite size. Our previous calculation\(^{[11]}\) based on the surface/bulk nucleation and growth model of Villa and Rios\(^{[19]}\) also indicate that the reduction of particle size can result in the decrease of Avrami exponent in the JMAK model. Strictly speaking, for the particles with different sizes, the value of Avrami exponent used for JMAK model can be changed. While the value of Avrami exponent for all particles are assumed to be the same in this work, in the previous report, the value of Avrami exponent was set to be 4 for the limitation of the amount of data. In this work, JMAK models with Avrami exponent ranging from 0.5 to 4 were adopted for the fitting. As Figure 3 shows, the apparent activation energy increases with the decreasing Avrami exponent. The difference in the value of \( AE \) can be more than 5 times. The difference of \( R^2 \), the indicator of the quality of fitting, is tiny among the fitting results. Nevertheless, \( R^2 \) is a peak function of Avrami exponent. The optimized value of \( n \) is 1.405 with highest value of \( R^2 \), which is selected for the kinetic analysis. In the global fitting, the apparent activation energy for all the experiments is chosen to be the same. Moreover, the pre-exponential factor for the particles with the same size and in the same atmosphere is the same. Figure 4 shows the analysis results with the JMAK model \((n = 1.405)\). The value of apparent activation energy is estimated to be 105.5 kJ mol\(^{-1}\). The pre-exponential factors are listed in Table II.

### B. Effect of Temperature on the Reduction Process

The Arrhenius equation is employed to describe the relationship between the reaction rate constant and temperature in this process. The value of \( AE \) in this work is lower than that in the report of Qu et al.\(^{[8,10]}\) It is in that the reaction mechanism changes due to the temperature elevation. The difference in resources of raw materials could also contribute to the various kinetic mechanisms. There are a lot of activation energy data in the literature with the reaction temperature lower than 1273 K. The summarization from the recent reports\(^{[20,21]}\) indicated that the value of the activation energy varied from 33.3 to 139.2 kJ mol\(^{-1}\) for the reduction of Fe\(_2\)O\(_3\) in H\(_2\) or CO containing atmospheres. The only comparable results in the similar high-temperature range are from the research group of Sohn. Their reports indicated that the activation energy of H\(_2\) or CO reduction of hematite particles was 214 and 231 kJ mol\(^{-1}\), respectively.\(^{[22,23]}\) Sohn et al. also reported the kinetic mechanism of magnetite concentrate at high temperature in the form of the JMAK model. The value of \( n \) varies from 2\(^{[24,25]}\) to 0.56\(^{[26]}\) under different experimental conditions. Moreover, the \( AE \) of the reduction ranges from 180 to 463 kJ mol\(^{-1}\).\(^{[24,25,27,28]}\) The value of kinetic parameters highly depends on the structure of the reagent and the reaction conditions.\(^{[29,30]}\) For instance, Pourghahramani et al.\(^{[31]}\) reported that introducing dislocations and defects into the mineral structure could reduce the activation energy of the reduction. Therefore, the reported value in this work is in reasonable range.

Table I. Atmospheres in the Experiments

| Atmosphere | CO (Vol Pct) | CO\(_2\) (Vol Pct) | H\(_2\) (Vol Pct) | N\(_2\) (Vol Pct) |
|------------|--------------|-------------------|-----------------|-----------------|
| PCR2\(^{'}\) | 45           | 55                | 0               | 0               |
| PCR4\(^{'}\) | 5            | 95                | 0               | 0               |
| PCR2       | 35.58        | 31.73             | 4.81            | 27.88           |
| PCR4       | 4            | 66                | 1               | 29              |

Fig. 1—Reduction degree of hematite ore particles in this work which is calculated from chemical analysis and XRD results. A parabola can represent this relationship. Different symbols here indicate data from different batches of experiments.
C. Effect of Heat Transfer on the Reduction Process

Due to the global fitting needs to develop a balance among the errors of all batches of experimental data, one could find the deviation of the fitting curves from a part of the raw data. Nevertheless, it can be noted in Figure 4 that the deviation of the experimental data of 244 \( \mu \text{m} \) particle from the modeling result is relatively significant. The four data points with \( R^2 \) around 0.73 in the two box charts with data in Figure 3 are corresponding to the experimental data of 244 \( \mu \text{m} \) particle. On the one hand, the reduction degree of 244 \( \mu \text{m} \) particle is much lower than the other particles. It results in a significant relative error of the experimental data. On the other hand, the extremely low values of \( R^2 \) also imply a deviation of the reaction process of 244 \( \mu \text{m} \) particle from other particles. It is suspected to be the effect of heat transfer during the reaction. This will be discussed in the following sections.

Although the reduction is regarded as an isothermal reaction in the kinetic analysis, the heating process of hematite particles from room temperature to the reaction temperature needs a certain period of time when it is suddenly injected into the heating zone of the furnace. The heating-up time could be longer for the large particles, and the slow heating process can delay the reduction of hematite. In order to confirm this hypothesis, a simplified calculation was employed for the analysis of the heat transfer process of a hematite particle in terms of characteristic heating times.

Heat conduction was considered as the heat transfer mode within the particle. Convection and radiation were considered in the heat transfer in the CO\(_2\) atmosphere. The influence of the enthalpy change of chemical reactions is not considered during the calculation. The parameters in the calculation are listed in Table III. Especially, the surface emissivity of the ore and wall is a suggested value for chalcopyrite \[^{32}\]. With the assumption that the particles are spheres, the characteristic time of the three modes of heat transfer are as follows \[^{33}\]:

Gas phase conduction:

\[
t_c = \frac{\rho_p C_p d_p^2}{6Nu \kappa_g}
\]  

[7]

Radiation:

\[
t_r = 0.42 \frac{\rho_p d_p C_p}{12 \sigma T_w^3} \left( \frac{T_p^0}{T_w} \right)
\]  

[8]

Conduction inside the particle:

\[
t_{c,p} = 2 \frac{\rho_p C_p d_p^2}{20 \kappa_p}
\]  

[9]

At the characteristic time, the temperature of one particle (or the geometrical center of the particle in Eq. [9]) has been raised to 1251 K, which is 0.632 times of the difference between its initial temperature and ambient temperature.

Figure 5 shows the calculation results which show that the characteristic time of internal conduction of the particle is always lower than 70 ms, which is much lower than the other two characteristic times. Hence temperature distribution within the particle during the reaction can be treated as uniform, since heat transfer resistance is located outside the particle. The figure also shows that the principal mode of heat transfer from the ambiance to the small particles is conduction, and to the large particles is radiation. Generally, the characteristic time of heat transfer from ambiance to the particle varies from less than 100 ms to more than 1000 ms with the increase of particle size. For instance, the value of \( t_c \) is as high as 583 ms for 500 \( \mu \text{m} \) particle. This value is longer than the residence time of it in HTDF. It indicates that the reduction of 244 \( \mu \text{m} \) particles is non-isothermal, and error of the prediction results of kinetic modeling, which is based on isothermal reactions. Besides, it verifies that the reduction of small particles (\( d_p \leq 142 \mu \text{m} \)) can be simplified as an isothermal reaction in the present work.
D. Effect of Particle Size on the Reduction Process

The effect of particle size on the reaction rate constant has been discussed in detail in our previous work [11] which reported that the reduction rate of the particles with particle size of 85 \( \mu m \) reached the highest, while quadratic equations were adopted for the description of the effect of particle size on the reduction process at 1735 K:

\[
A = \begin{cases} 
  (0.21 \sim 0.23) \times 10^{12}d^2, & d \leq 85 \mu m \\
  (0.17 \sim 0.19) \times 10^{-2}d^{-1}, & d \geq 85 \mu m 
\end{cases}
\]

Table II. Pre-Exponential Factors (s\(^{-1}\)) in JMAK Model (\( \eta = 1.405, E = 105.5 \text{ kJ/mol} \)) as the Fitting Results

| Atmosphere | 67 \( \mu m \)  | 85 \( \mu m \)  | 110 \( \mu m \) | 142 \( \mu m \)  | 244 \( \mu m \)  |
|------------|-----------------|-----------------|---------------|-----------------|-----------------|
| PCR4'      | 9294 ± 814      | ≥ 58,500*       | 44450 ± 7140  | 14120 ± 1510    | 5039 ± 198      |
| PCR2'      | 11310 ± 1060    | ≥ 57,700*       | 30110 ± 1950  | 19370 ± 2930    | 3547 ± 387      |
| PCR4       | 25510 ± 6010    |                | 25510 ± 6010  | 25510 ± 6010    | 25510 ± 6010    |
| PCR2       | 48180 ± 30840   |                | 48180 ± 30840 | 48180 ± 30840   | 48180 ± 30840   |

*It is the lower limit of the pre-exponential factor
where the units of $A$ and $d$ are s$^{-1}$ and m, respectively, the particle size $d$ is in the range of 67 to 244 μm. It was suggested that, based on the JMAK model with Avrami exponent as 4, the theoretical equation for reaction rate was suggested to be an inverse proportional function of particle size when the particle size is larger than 85 μm. The original theoretical elaboration of this relationship is from the classical work of Mampel. It is noted that the experimental data were employed more in this work, covering the temperature from 1710 K to 1786 K. Therefore, with a larger database and the same global fitting method, the Avrami exponent in the JMAK model was further optimized to be 1.405 in the present work, and the relationship of reaction rate constant and particle size was examined with more extensive data.

As Figure 6 demonstrates, the reaction rate constant of 110 μm particle is higher than that of 67 μm particle in the temperature range from 1710 K to 1786 K. Kinetic Models for nucleation and growth process also indicates that the increasing particle size of “small” particles can facilitate reaction rate of them. It verifies that the reduction of hematite is rate-determined by the nucleation and growth process in this work. Furthermore, an empirical formula can be established for the particles with a size larger than 110 μm:

\[
A = \begin{cases} 
(0.9 \pm 2.5) \times 10^9 d^{-2.2 \pm 0.5}, & \text{for PCR2'} \\
(1.4 \pm 5.5) \times 10^{13} d^{-4.2 \pm 0.8}, & \text{for PCR4''} 
\end{cases}
\]

where the units of $A$ and $d$ are s$^{-1}$ and m, respectively (Figure 7).

E. Effect of Oxygen Partial Pressure on the Reduction Process

Wang et al. proposed that the effect of gas on the reaction rate constant of magnetite concentrate can be described as:

\[
k \propto \rho_{H_2O}^{1/2} - (p_{H_2O}/K)^{1/2},
\]

where the units of $k$ and $p$ are s$^{-1}$ and atm, respectively. Fan et al. suggested that the reaction rate constant of magnetite concentrate has a linear relationship with the partial pressure of hydrogen and water vapor in the reacting gas. Their studies were in the environment of humidified hydrogen. Additionally, Post Combustion Ratio (PCR) is used in industrial practice, where the PCR of gas is defined as follows:

\[
\text{PCR} = \frac{p(\text{CO}_2) + p(\text{H}_2\text{O})}{p(\text{CO}_2) + p(\text{H}_2\text{O}) + p(\text{CO}) + p(\text{H}_2)} \times 100\%.
\]

The test results of HIsarna experimental plant implies that, roughly, the reduction degree of the cyclone production has a linear relationship with the PCR value of the reacting gas. Similarly, Qu suggested in her thesis that the reaction rate constant of hematite as solid or solid-liquid-mixture particles follows a linear relationship with $p(\text{CO}) + p(\text{H}_2)$ under her experimental conditions:

\[
k = A + B \frac{p(\text{CO}) + p(\text{H}_2)}{p(\text{total})},
\]

where $p(\text{total})$ is the pressure of the total gas, $A$ and $B$ are constant. There are different values for $A$ and $B$ in different atmospheres. The only exception is the reduction of solid-liquid-mixture particles of hematite in $\text{H}_2-\text{CO}-\text{CO}_2-\text{N}_2$ gas at 1650 K. It can be noted that Eq. [14] is a specialized form of the effect of PCR on the reaction rate constant. In the present work, the partial pressure of oxygen was introduced into the formula instead of PCR value. As Figure 8(a) shows, it is easy to infer a linear relation of $k$ and $p(\text{O}_2)$ for different atmospheres:

\[
\begin{aligned}
& k = -(0.084 \pm 0.006) - (0.0056 \pm 0.0003) \ln p(\text{O}_2), & \text{for gas-solid reaction} \\
& k = -(0.259 \pm 0.003) - (0.0019 \pm 0.0002) \ln p(\text{O}_2), & \text{for gas-mixture reaction}
\end{aligned}
\]

The same as the report of Qu, there is an exception to the data point, which is lower than the predicted value. Nevertheless, it can be realized that the effect of different gas compositions on the reaction rate constant can be summarized as the function of $p(\text{O}_2)$. The same trends can be found in our study for the particles with an average size of 67 and 142 μm. The reaction rate constant decreases with the increase of $p(\text{O}_2)$ for these reduction processes. However, there is an abnormal relationship between $k$ and $p(\text{O}_2)$ for the reduction of 110 μm particles. The following hypothesis is proposed, which could explain the unusual phenomenon of the reduction of 110 μm particles: if the reduction rate of the ore particles is fast enough, the heating-up process can be one of the determining factors of the reaction rate. The following details are the support of this hypothesis.

It is known that the reduction of hematite ore is composed of two parts of reactions: thermal decomposition and gas reduction. Based on the published experimental data of Qu, the participation of the two reactions in the reaction process is estimated through her model. The illustration results are presented in Figure 9. It shows that the principal reaction is thermal decomposition at initial, and it accomplished within 200 ms. The rate of gas reduction is lower than the thermal decomposition at the beginning, while the gas reduction dominates the following process. The thermal decomposition time has also been evaluated for our samples. Figure 10 shows the kinetic data of thermal decomposition of hematite ore. It can be noted that the fast reaction accomplished within 70 ms at 1785 K in the $\text{N}_2$ atmosphere. The reaction rate is comparable with the reaction rate of the same particles in PCR4’ gas. A JMAK model with Avrami exponent of 1.405 was also employed to fit the experimental data. The modeling results show that the reaction rate constant is 32.7 ± 7.1 s$^{-1}$, and the reduction degree of the ore at the terminal point is 12.3 ± 0.4 pct. It reconfirms that the reaction rate of thermal decomposition is high enough.
comparing to the overall reaction rate. It also implies that the reduction process of hematite ore particles in PCR4 gas, or the atmosphere with low reducing potential, can be dominated by the thermal decomposition reaction. Therefore, the inverse trends of the reaction rate of 110 μm particles in Figure 8 are because of the character of thermal decomposition. Qu et al. observed that the equivalent reduction degrees and reduction degree of hematite in CO2 is higher than that in Ar and N2 in the thermal decomposition process. It is suggested to be the radiative properties of CO2 gas. The heat transfer in CO2 gas is more effective than that in Ar and N2. Due to the slower heat up process in Ar and N2 gases, the corresponding reduction rates are lower. Similarly, in our work, the reduction degree of hematite particles in pure CO2 at 1710 K can reach the same value of the ore in N2 gas and in 69.5 vol pct CO2 + 30.5 vol pct N2 gas.

| Parameter                        | Symbol     | Value       |
|----------------------------------|------------|-------------|
| Density of Ore                   | $\rho_p$ (kg m$^{-3}$) | 5240        |
| Heat Capacity of Ore             | $C_p$ (J kg$^{-1}$ K$^{-1}$) | 1000$^{[34]}$ |
| Conductivity of Ore              | $\lambda_p$ (W m$^{-1}$ K$^{-1}$) | 1$^{[34,35]}$ |
| Diameter of Ore                  | $d_p$ (μm) | 30 to 500   |
| Initial Temperature of Ore       | $T_{p_0}$ (K) | 355        |
| Temperature of Tube/Ambience     | $T_w$ (K) | 1773        |
| Pressure                         | $P$ (atm) | 1           |
| Nusselt Number                   | $\varepsilon_p$ | 0.5        |
| Surface Emissivity of Ore/Wall   |            |             |

Fig. 5—Characteristic time of the heating-up process of particles with different sizes.

Fig. 6—Effect of particle size on the reaction rate constant in (a) PCR4’ and (b) PCR2’ atmospheres.
at 1785 K. Moreover, Figure 10 also indicates that, although pure CO\textsubscript{2} can effectively accelerate the heat transfer process, even as high as 69.5 vol pct of CO\textsubscript{2} cannot significantly raise the reduction degree of ore in thermal decomposition. As shown in Figure 8(c), it can be noted that the reaction rate constants of hematite particles in PCR4\textsuperscript{¢} gas are higher than those in PCR2\textsuperscript{¢} gas for the 110 \textmu m particles. Yet, the value of \( k \) decreases with the increase of \( p(\text{O}_2) \) in PCR2, PCR2\textsuperscript{¢} and PCR4 gases at 1785 K in sequence. The CO\textsubscript{2} concentration in PCR4\textsuperscript{¢} gas is 95 vol pct, and it in other gases is lower than 69.5 vol pct. That implies that the effect of CO\textsubscript{2} on the heating-up process of ore particles is less strong in the other three gases. Therefore, only the reaction of 110 \textmu m particles in PCR4\textsuperscript{¢} gas performs “abnormal” high reaction rate. It results in the different trend for 110 \textmu m particles in Figure 8. Besides, we have not discussed the reaction rate constants of 85 \textmu m and 244 \textmu m particles because of the large error bars of them.

**IV. CONCLUSIONS**

The reduction kinetics of hematite ore particles at the temperature ranging from 1710 K to 1785 K has been investigated in this work.

(1) The reduction rate of hematite ore particles is determined by the nucleation and growth process during the reaction, which follows the JMAK model in the form of

\[
-\ln \left(1 - \frac{R}{R_{\text{max}}} \right) = -\left[ A \exp \left(\frac{-105.5 \times 10^3}{R_g T} \right) \right]^{1.405} t.
\]

(2) The effect of the partial pressure of the gas and the reaction temperature on the reduction degree of hematite ore particles at the terminal point is described by the following equations:

**Fig. 7—Relationship between particle size and pre-exponential factor.**

**Fig. 8—Effect of partial pressure of oxygen on reaction rate constant for (a) experimental data in Ref. [10]; (b) the reaction of 67 \textmu m and 142 \textmu m particles; and (c) the reaction of 110 \textmu m particles.**

\[
R_{\text{max}} = (-165 \pm 25) + (8.62 \pm 1.41) \times 10^{-2} T - (2.16 \pm 0.14) \ln p(\text{O}_2)
\]
radiation to gas phase conduction with the increase of particle size. Moreover, the heating-up process of large particles, extremely 244 μm particles in this study, could have a negative effect on the reduction degree. (4) It is indicated that the pre-exponential factor, $A$, is a peak function of reacting particle size, with a maximum value at around 85 μm. Moreover, the value of $A$ can be expressed as an exponential function of particle size in the range between 110 μm and 244 μm at 1735 K:

$$A = (0.9 \pm 2.5) \times 10^9 d^{-(2.2 \pm 0.5)}, \quad \text{for PCR2'}$$

$$A = (1.4 \pm 5.5) \times 10^{13} d^{-(4.2 \pm 0.8)}, \quad \text{for PCR4'}$$

(5) When the reaction is dominated by gas reduction, the reaction rate constant linearly decreased with the increase of $\ln[p(O_2)]$ in the reacting gases. The reaction of hematite particles within 70 ms can be dominated by the thermal decomposition rather than the gas reduction. Furthermore, the reaction rate of thermal decomposition can be accelerated by increasing the radiative properties of the gas mixture, which is introducing high content of CO$_2$ into the gas system. As a result, within the scope of the investigation, the reduction rate of 110 μm hematite particles in 95 pct CO$_2$-containing gas is higher than that in the other less CO$_2$-containing gas mixtures.

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