SVDistNet: Self-Supervised Near-Field Distance Estimation on Surround View Fisheye Cameras

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Abstract—A 360° perception of scene geometry is essential for automated driving, notably for parking and urban driving scenarios. Typically, it is achieved using surround-view fisheye cameras, focusing on the near-field area around the vehicle. The majority of current depth estimation approaches focus on employing just a single camera, which cannot be straightforwardly generalized to multiple cameras. The depth estimation model must be tested on a variety of cameras equipped to millions of cars with varying camera geometries. Even within a single car, intrinsics vary due to manufacturing tolerances. Deep learning models are sensitive to these changes, and it is practically infeasible to train and test on each camera variant. As a result, we present novel camera-geometry adaptive multi-scale convolutions which utilize the camera parameters as a conditional input, enabling the model to generalize to previously unseen fisheye cameras. Additionally, we improve the distance estimation by pairwise and patchwise vector-based self-attention encoder networks. We evaluate our approach on the Fisheye WoodScape surround-view dataset, significantly improving over previous approaches. We also show a generalization of our approach across different camera viewing angles and perform extensive experiments to support our contributions. To enable comparison with other approaches, we evaluate the front camera data on the KITTI dataset (pinhole camera images) and achieve state-of-the-art performance among self-supervised monocular methods. An overview video with qualitative results is provided at https://youtu.be/bmX0UcU9wpA. Baseline code and dataset will be made public.

Index Terms—Depth estimation, semantic segmentation, fisheye cameras, surround-view, multi-task learning, neural networks, self-supervised learning.

I. INTRODUCTION

Surround View Cameras Typically, automotive perception systems use multiple cameras, with current systems having at least four cameras. The number is likely to increase to more than ten cameras for future generation systems. Such surround-view cameras are focused on near field sensing, which is typically used for low-speed applications such as parking or traffic jam assistance functions [1]. Fig. 1 shows sample distance estimation images of four cameras mounted on a car covering the entire 360° field of view surrounding the car. Near-field distance estimation is a challenging problem because of distortion and partial visibility of close-by objects [2]. Also, centimeter-level accuracy is required to enable precise low-speed maneuvers such as parking. Up to now, for the generation of high-quality distance estimates, one network per camera has to be trained, inducing unfeasible computational complexity with an increasing number of cameras.

Motivation of SV DistNet Our work’s primary motivation is to propose a solution for surround-view fisheye cameras targeting large-scale industrial deployment. In other words, we aim to develop a model that is applicable to a vast number of automated driving vehicles possessing their own set of cameras. However, the underlying camera intrinsics are not even entirely identical for a given vehicle family. There are differences due to manufacturing processes that lead to a separate calibration of each camera instance. Calibration can vary even after deployment due to high environmental temperatures or aging. As a result, we require a calibration adaptation mechanism in the model. This contrasts with public datasets, which employ a single camera instance for both training and testing. There are 12 different cameras with slight intrinsic variations in the WoodScape dataset [3] to assess this effect. There are 4 camera instances around the vehicle with
varying intrinsics, even for a single instance of a surround-view system. Instead of having four separate models for each camera, we, therefore, propose a single model for all cameras, which has advantages such as (i) a lower memory footprint and a better data transmission rate leading to improved efficiency, (ii) a better regularization during training due to the wider variety of different cameras in a more extensive training dataset, and (iii) an easier to handle maintenance of just a single neural network model instead of multiple ones.

Recently proposed methods for self-supervised depth estimation [4], [5], [6] present a powerful tool for the perception of scene geometry from camera images as they are trainable on arbitrary image sequences. While initial methods mainly focused on pinhole cameras [7], [5], [8], for practical deployment, the more general distance estimation [9], [10] on other camera geometries such as fisheye cameras are of significant interest due to their large field of view. There are many benefits in using raw images instead of undistortion, refer to [10] for details. Moreover, current methods essentially focus on single front-view camera systems, while the question of how to extend such models to multiple cameras is essentially left open. Therefore, in this work, we extend our previous synergized multi-task learning method for self-supervised distance estimation and semantic segmentation [11] to a general application on surround-view cameras and propose additional improvements.

To sum up, our contributions are as follows:

- We present a novel camera geometry adaptive multi-scale convolution to incorporate the camera parameters into our self-supervised distance estimation framework. We feed this camera geometry tensor representation to the model as a generic way to adapt to new camera intrinsics.
- We create a training framework for self-supervised distance estimation, which jointly trains and infers images from multiple fisheye cameras and viewpoints.
- We demonstrate a single model for 12 fisheye cameras, which achieves the equivalent result as an individual specialized model that overfits a particular camera model.
- We present an improved version of our network architecture for multi-task learning of self-supervised distance estimation and semantic segmentation. We significantly improve upon our previous works FisheyeDistanceNet [9], UnrectDepthNet [10], and SynDistNet [11].
- We achieve state-of-the-art results on the WoodScape and KITTI datasets among monocular self-supervised depth estimation methods.

II. RELATED WORK

This section provides a survey regarding self-supervised depth estimation and, in particular, its applications to different camera geometries. Also, we discuss the application of self-supervised depth estimation in multi-task learning approaches and approaches using semantic guidance for this task.

**Self-Supervised Depth Estimation** Training a neural network to predict a depth map by optimizing this depth map as a parameter of geometric projections between stereo images or sequential images has been defined as the task of self-supervised depth estimation [4]. For performance gains, the following approaches extended the fundamental concept by improved loss functions [12], [5], or network architectures, optimized for the task of depth estimation [13]. Concurrently, it was proposed to use proxy labels from traditional stereo algorithms [14]. To better model the structural information from the temporal context, recurrent neural networks were employed [15], [16], and Casser et al. [7], [17] introduced a test-time refinement method to improve the network performance in an online manner. While all of these approaches achieve significant results on pinhole camera images, they are seldom transferred to more complex camera models, *e.g.*, fisheye camera images. In contrast, we exhibit our self-supervised distance estimation method’s applicability on both pinhole and fisheye camera images.

**Multi-Task Learning** Exemplary tasks, which benefit from multi-task learning, *i.e.*, share some of the network parts, in terms of performance and efficiency are, *e.g.*, depth estimation [18], [19], semantic segmentation [20], [21], [19] and domain adaptation [22]. As an empirical weighting of the losses involves extensive hyperparameter tuning, we follow the uncertainty-based weighting of Kendall et al. [18] to weigh the different tasks. To handle dynamic objects during training that violate the static world assumption in the projections of the self-supervised depth estimation, it is common to additionally estimate optical flow, which can also be trained in a self-supervised fashion [23]. Through this simultaneous estimation of both outputs, it is thereby plausible to enforce cross-task consistency [24], to modify the projected image and correct the influence of dynamic objects [25], or to enforce prior known geometric constraints. Although optical flow is the commonly used technique to handle dynamic objects, we consider an alternative method, introduced by [8], [11] because, firstly, semantic segmentation is a task that is readily available in most autonomous driving systems and, secondly, optical flow is computationally more complex and hard to validate due to the extensive effort needed to obtain ground truth.

**Semantically-Guided Depth Estimation** Complementing self-supervised depth estimation by the additional prediction of semantic or instance segmentation in cross-task guidance approaches has been shown to increase the performance of both prediction modalities [7], [17], [8], [26], [27], [28]. Either the segmentation masks are given as an additional input to the network [28], or they are used to predict relative poses for the single dynamic objects to counterpoise their movement between consecutive frames [7], [17]. While primary approaches used a pre-trained segmentation network, it was also shown that both tasks could be trained simultaneously [29], [30]. Thereby, it is possible to project the segmentation outputs between consecutive frames and enforce temporal semantic consistency [29], [31], or enforce edge consistency across the different output modalities [29], [30]. In this work, we use the segmentation output to identify dynamic objects and handle them accordingly inside the photometric loss as in [8], [11]. Additionally, we propose a multi-task network, where the encoder is based on pairwise and patchwise self-attention networks together with pixel-adaptive convolutions inside the decoder (as in [28]), which can be trained in a single-stage manner, eliminating the need for a pre-trained segmentation network.
network compared to [28].

**Depth Estimation for Different Camera Geometries**

Employing self-supervised depth estimation techniques to different camera geometries than a single pinhole camera is challenging for two reasons. Firstly, the intrinsic camera parameters are assumed to be constant for all images. Secondly, the viewing angle is assumed to be constant for all camera images, as usually only a front-facing camera is considered (e.g., [4], [5]). Gordon et al. [32] predicts not only the relative pose but also the intrinsic camera parameters, enabling the generalization across images from different pinhole cameras. Meanwhile, Facil et al. [33] introduces a method to give the intrinsic camera parameters an additional input to the convolution operation, showing the same effect. In this work, we transfer the approach [33] to fisheye camera images, thereby enabling generalization of our distance estimation method across different fisheye cameras and viewing angles.

The transfer of self-supervised depth estimation to the more general self-supervised distance estimation on camera geometries, such as, e.g., fisheye cameras, was introduced by Ravi Kumar et al. [9], [10], which focus on front-view cameras. Surround-view depth coverage has also been shown by [34], [35], which applies self-supervised depth estimation techniques to 360° images. In this work, we do not have to impose a 360° image in advance to the model; we enable a surround-view coverage of geometric information for an autonomous vehicle by applying the same neural network to many arbitrary cameras with different viewing angles.

**III. Multi-Task Learning Framework**

This section describes our multi-task learning framework for collaborative distance and semantic segmentation prediction, which we apply to surround-view camera systems. The learning framework is based on our previous work FishEyeDistanceNet [9], UnrectDepthNet [10], and SynDistNet [11] with extensions to support multiple cameras. To enable comparison, we use the same protocols and losses.

**A. Self-Supervised Distance and Pose Estimation**

We develop our single-image distance and pose estimation framework for multiple cameras building on our previous work FishEyeDistanceNet [9], where we outlined the basic mechanism of our polynomial projection model for fisheye cameras. Accordingly, the total loss for our distance and pose estimation networks (cf. Fig. 2) consists of a image reconstruction contribution $L_r$, minimizing the difference between the reconstructed images $\hat{I}_{t'\rightarrow t}$ and the target frames $I_t$ and a regularizing contribution $L_s$, enforcing edge-aware smoothness as outlined in [12]. Additionally, we make use of the cross-sequence distance consistency loss $L_{dc}$, as well as the scale recovery technique from [9]. The total loss is averaged over image batches, scales, and pixel locations and is given as

$$L_{tot} = L_r(I_t, \hat{I}_{t'\rightarrow t}) + \beta L_s(\hat{D}_s) + \gamma L_{dc}(\hat{D}_s, \hat{D}_{t'})$$

(1)

with $\beta$ and $\gamma$ being constants, weighing the influence of the regularization term $L_s$ and the cross-sequence distance consistency term $L_{dc}$, respectively.

**Image Reconstruction Loss**

The majority of cutting-edge self-supervised depth estimation approaches use heuristic loss functions. The optimal selection of a loss function, on the other hand, is not well defined theoretically. We emphasized the importance of investigating a better reconstruction loss in our previous paper, SynDistNet [11]. We incorporated Barron’s [36] more generic robust loss function, which was used to replace the $L_1$ term employed in [9], [10], [12], [5]. In the context of distance/depth estimation, we presented the common notion of a per-pixel regression $\rho$, indicated by

$$\rho(\xi) = \rho(\hat{I}_{t} - \hat{I}_{t'\rightarrow t})$$

(2)

This robust loss function generalizes several common losses, including the $L_1$, $L_2$, Geman-McClure, Welsch/Leclerc, Cauchy/Lorentzian, and Charbonnier loss functions. Robustness is introduced as a continuous parameter that can be optimized within the loss function to increase regression task performance. The robust loss function $\rho_{rob}$ is as follows:

$$\rho_{rob}(\xi) = \frac{|\alpha - 2|}{\alpha} \left( \frac{(\xi/\alpha)^2}{(\alpha - 2)} + 1 \right)^{\alpha/2} - 1$$

(3)

As described in [36], one can use a data-driven optimization to automatically adapt the free parameters $\alpha$ and $c$ to the investigated problem. The image reconstruction loss between the target frame $I_t$ and the reconstructed target frame $\hat{I}_{t'\rightarrow t}$ is computed by a mixture of the Structural Similarity loss term and the robust pixel-wise loss term as

$$\rho_{rob}(\xi) = \rho \left( \left( I_t - \hat{I}_{t'\rightarrow t} \right) \odot M_{t\rightarrow t'} \right)$$

(4)

$$\tilde{L}_r(I_t, \hat{I}_{t'\rightarrow t}) = \frac{1}{2} \left( \frac{1}{\tau} - \text{SSIM}(I_t, \hat{I}_{t'\rightarrow t}, M_{t\rightarrow t'}) \right)$$

(5)

$$\rho_{rob}(\xi) = \rho \left( \left( I_t - \hat{I}_{t'\rightarrow t} \right) \odot M_{t\rightarrow t'} \right)$$

(6)

**B. Semantic Guidance for Image Reconstruction Loss**

To improve distance estimation performance through handling dynamic objects accordingly, in this part, we describe how we train our semantic segmentation baseline and afterward describe the semantic masking technique incorporated from our previous work [11] to exclude their influence on the reconstruction loss.

**Semantic Segmentation Baseline:** Semantic segmentation aims at assigning a class label $s$ from a subset of classes $s \in S = \{1, 2, ..., S\}$. The desired output is then a pixelwise semantic segmentation mask $M_t$ with the same spatial dimensions as the segmentation network’s input $I_t$. During training, the network predicts posterior probabilities $Y_{t}$, representing the likelihood that a pixel belongs to a class $s \in S$. 

$$L_r = \min_{t'} \tilde{L}_r(I_t, \hat{I}_{t'\rightarrow t})$$

(6)
Fig. 2: High-level overview of our surround-view self-supervised distance estimation framework, which employs semantic guidance as well as camera-geometry adaptive convolutions (orange blocks). Our framework comprises training units for self-supervised distance estimation (blue blocks) and semantic segmentation (green blocks). The camera tensor \( C_t \) (orange block) assists our SVDistNet in producing distance maps across multiple camera- viewpoints and making the network camera independent. As explained in Section IV-A, \( C_t \) can also be applied to standard camera models. The multi-task loss from 9 weights and optimizes both modalities at the same time. By post-processing the predicted distance maps in 3D space, we can obtain surround-view geometric information using our proposed framework.

We mask dynamic objects by multiplying the mask with the reconstruction loss from Eq. 4 in a pixel-wise fashion. However, there are images in which these dynamic objects are not moving, e.g., parking cars are perfect to learn the distance of cars, while cars on a highway severely violate the static world assumption. Accordingly, we want to learn the distance of moving dynamic objects by learning from images, in which they are detected as non-moving. As a result, we detect images with non-moving dynamic objects using a semantic consistency measure introduced in our previous works [8], [11] and only mask the dynamic objects in a fraction epsilon of images where dynamic objects are detected as mostly moving.

C. Joint Optimization

Based on Kendall’s et al. [18] task weighting strategy, the distance estimation and semantic segmentation loss terms from Eq. 1 and Eq. 7, respectively, are weighted. The total optimization objective is derived from [11].

\[
\frac{1}{2\sigma_1^2}L_{tot} + \frac{1}{2\sigma_2^2}L_{ce} + \log(1 + \sigma_1) + \log(1 + \sigma_2) \tag{9}
\]

where \( \sigma_1 \) and \( \sigma_2 \) are learnable parameters introduced to optimize the homoscedastic uncertainty. The goal is to optimize a more substantial uncertainty, resulting in a smaller contribution of the loss from the distance estimation or semantic segmentation task to the total loss. It is important to note that the respective task’s weight is reduced by increasing the noise parameter \( \sigma \). We observe that the noise parameter \( \sigma_1 \) of the distance estimation task is lower than \( \sigma_2 \) of semantic segmentation, and over time, the convergence occurs correspondingly.
Our encoder is a self-attention network with pairwise and patchwise shared vector-based self-attention encoder and task-specific decoders. We intend to convert all the camera geometry characteristics incorporating camera geometry into the distance estimation. This is an unsolved problem, and we aim to solve this by developing a single model for all cameras, as discussed in the introduction.

Different fields of view. Instead of developing an individual radial distortion models: 1) Polynomial: \( \psi(\vartheta) = a_1 \vartheta + a_2 \vartheta^2 + a_3 \vartheta^3 + a_4 \vartheta^4 \)
2) UCM: \( \psi(\vartheta) = f \cdot \sin \vartheta / (f \cdot \vartheta + \xi) \)
3) eUCM: \( \psi(\vartheta) = f \cdot \sin \vartheta / (f \cdot \vartheta + \alpha \sqrt{\sin^2 \vartheta + \cos^2 \vartheta - \cos \vartheta}) \)
4) Rectilinear: \( \psi(\vartheta) = f \cdot \tan \vartheta \)
5) Stereographic: \( \psi(\vartheta) = 2f \cdot \tan(\vartheta/2) \)
6) Double Sphere: \( \psi(\vartheta) = f \cdot \frac{\sin \vartheta}{\alpha \sqrt{\sin^2 \vartheta + (\xi + \cos \vartheta)^2} + (1-\alpha)(\xi + \cos \vartheta)} \)

The distortion coefficients \( a_x, a_y, a_3, a_4 \) are used to create the angle of incidence maps \( (x, y, a_x, a_y) \), and the camera’s sensor dimensions (width \( w \) and height \( h \)) are used to formulate the are utilized to formulate the normalized coordinate maps. We compute these maps using the camera intrinsic parameters and include them in our shared self-attention decoder from [11] to facilitate the distance decoder. Thereby, an adaptation of the weights across spatial and channel dimensions is implemented. We retain our semantic guidance decoder from [11] to facilitate the distance decoder to yield accurate distance predictions. The complete training of both tasks is performed in a one-stage manner.

A. Camera Geometry Tensor \( C_t \)

Automated driving systems have a wide variety of cameras, typically around 10, placed in different car locations and with different fields of view. Instead of developing an individual model for each camera, it is highly desirable to develop a single model for all cameras, as discussed in the introduction. This is an unsolved problem, and we aim to solve this by incorporating camera geometry into the distance estimation. We intend to convert all the camera geometry characteristics into a tensor called camera geometry tensor \( C_t \) and provide this as input to the CNN model at both training and inference. From the view of distance estimation, camera intrinsics is the primary model adaptation needed. However, the camera tensor notion is generic, and we plan to extend it to include camera extrinsics and camera motion (visual odometry) for improving other tasks. CAM-Convs [33], which utilizes camera-aware convolutions for pinhole cameras, is the closest work. We extend and generalize this work to arbitrary camera geometries, including fisheye cameras.

The camera geometry adaptive mechanism is fundamental in the training process of the SVDistNet as the four different cameras mounted on the car have different intrinsic parameters and viewpoints. The trained distance and pose estimation networks need to generalize when deployed on a different car with a change in multiple viewpoints and intrinsics. To accomplish this, as shown in Fig. 3, we include the camera geometry tensor \( C_t \) in the mapping from RGB features to 3D information for distance estimation and semantic segmentation. In addition, as shown in Fig. 2, we add \( C_t \) to the pose encoder.

The tensor \( C_t \) can be obtained using a three-step procedure: First, we pre-compute pixel-wise coordinates and the angle of the incidence maps to facilitate a more efficient training. To incorporate the knowledge encoded in these camera calibration parameters, the normalized coordinates per pixel are used as additional channels and concatenated, yielding the tensor \( C_t \). Finally, these features are passed along with the encoder features to our SAN pairwise and patchwise models. Accordingly, we have six additional channels, supplementing the existing decoder channel inputs. In theory, the proposed method can be applied to any given fisheye projection model. We briefly present the standard projection models that our camera geometry tensor supports. The mapping of 3D points to pixels in fisheye lenses requires a radial component \( \psi(\vartheta) \). The polynomial model is the most commonly used, and more recent projection models include UCM (Unified Camera Model) [38] and eUCM (Enhanced UCM) [39]. Rectilinear (representation of a pinhole model) and Stereographic (mapping of a sphere to a plane) are not appropriate for fisheye lenses but are provided for comparison. The recently proposed Double Sphere model [40] has a closed-form inverse with low computational complexity. The following are summaries of the radial distortion models:

- Polynomial: \( \psi(\vartheta) = a_1 \vartheta + a_2 \vartheta^2 + a_3 \vartheta^3 + a_4 \vartheta^4 \)
- UCM: \( \psi(\vartheta) = f \cdot \sin \vartheta / (f \cdot \vartheta + \xi) \)
- eUCM: \( \psi(\vartheta) = f \cdot \sin \vartheta / (f \cdot \vartheta + \alpha \sqrt{\sin^2 \vartheta + \cos^2 \vartheta - \cos \vartheta}) \)
- Rectilinear: \( \psi(\vartheta) = f \cdot \tan \vartheta \)
- Stereographic: \( \psi(\vartheta) = 2f \cdot \tan(\vartheta/2) \)
- Double Sphere: \( \psi(\vartheta) = f \cdot \frac{\sin \vartheta}{\alpha \sqrt{\sin^2 \vartheta + (\xi + \cos \vartheta)^2} + (1-\alpha)(\xi + \cos \vartheta)} \)
attention encoder.

**Centered Coordinates (cc)** The SAN pairwise and patchwise operation modules receive the principal point position via the $cc_x$ and $cc_y$ coordinate channels, which are centred at $(0,0)$. We create $cc_x$ and $cc_y$ channels, as shown below:

$$cc_x = \begin{pmatrix} 0 - c_x \\ 1 - c_x \\ w - c_x \end{pmatrix}_{(w+1)\times 1}^\top \quad cc_y = \begin{pmatrix} 1 \\ 1 \\ h - c_y \end{pmatrix}_{(h+1)\times 1}^\top$$  \quad (10)

We concatenate $cc_x$ and $cc_y$ by resizing them with bilinear interpolation to match the input feature’s size.

**Angle of Incidence Maps ($a_x, a_y$)** Using the focal length $f$ of the camera, the horizontal and vertical angle of incidence maps for the pinhole (Rectilinear) camera model are determined from the $cc$ maps.

$$a_{ch}[i,j] = \arctan\left(\frac{cc_{ch}[i,j]}{f}\right)$$  \quad (11)

where $ch$ represents either $x$ or $y$ (see Eq. 10). By computing the inverse of the radial distortion functions $\rho(\vartheta)$, angle of incidence maps for different fisheye camera models can be calculated. The angle of incidence $\vartheta$ is computed numerically for the polynomial model employed in this paper by computing the $4^{th}$ order polynomial roots of $\vartheta = \sqrt{x_1^2 + y_1^2} = a_1 \vartheta + a_2 \vartheta^2 + a_3 \vartheta^3 + a_4 \vartheta^4$. To improve training efficiency, we store the pre-calculated roots in a lookup table for all pixel coordinates and generate the $a_x$ and $a_y$ maps by setting $x_f = cc_x[i,j], y_f = 0$ and $x_f = 0, y_f = cc_y[i,j]$, respectively. A lookup table is not necessary for UCM, eUCM, and Double Sphere projection models as they can be inverted analytically.

**Normalized Coordinates (nc)** Following [41], [33], we additionally introduce two channels of normalized coordinates, whose values span linearly with respect to the image coordinates between $-1$ and $1$. The channels are unaffected by camera sensor properties and characterize the spatial extent of the content in feature space in each direction (e.g., a $\hat{c}$ channel value close to $1$ indicates that the feature vector at this location is near the right border).

**B. Semantically-Guided Distance Decoder**

To better guide the distance features, we adapt the pixel-adaptive convolutions from [42], [28], thereby distilling the knowledge of the extracted features from the segmentation branch into the distance decoder. This follows the intuition that the distance estimation can profit from the location-specific knowledge encoded in the semantic features, which in return also breaks up the convolutions’ spatial invariance. While other semantic guidance approaches relied on a pretrained segmentation network, [7], [28], our semantic segmentation branch is learned simultaneously with the distance estimation, thereby introducing a more favorable one-stage training.

To implement the pixel-adaptive convolutions, we rely on the multi-level extraction of features from the segmentation decoder, as shown in Fig. 3. Accordingly, the input $x$ is processed as follows:

$$x'_{ij} = \sum_{ab\in N_k(i,j)} K(F_{ij}, F_{ab})W[r_{a-i,b-j}]x_{ab} + B$$  \quad (12)

where $r_{a-i,b-j}$ represents the distance between pixel locations $ij$ and $ab$ and $N_k(i,j)$ defines a neighborhood window of size $k \times k$ centered around the location $ij$. In Eq. 12, the elements of $x$ which are covered by the neighborhood window $N_k(i,j)$ make up the input to the convolution, characterized by a kernel function $K$, weights $W_i$, and a bias $B \in \mathbb{R}^1$. The kernel function is necessary to compute the correlation between the semantic features $F \in \mathbb{R}^D$ extracted by the segmentation decoder. Following [28], we define the kernel function as:

$$K(F_{ij}, F_{ab}) = \exp \left( -\frac{1}{2}(F_{ij} - F_{ab})^T \Sigma^{-1}_{ijab}(F_{ij} - F_{ab}) \right)$$  \quad (13)

where $\Sigma_{ijab}$ is the covariance matrix between the features $F_{ij}$ and $F_{ab}$. This matrix is chosen to be diagonal, which means that it can be expressed in terms of a learnable parameter $\sigma$ for each convolutional filter as $\sigma^2 \cdot 1^D$.

**V. IMPLEMENTATION DETAILS**

To minimise the training objective function, we use Pytorch to implement the models described in Section IV and the Ranger (RADam [43] + LookAhead [44]) optimizer. RADam uses an active rectifier to adjust Adam’s [45] adaptive momentum, resulting in an automated warm-up that is tailored to the dataset of interest. Meanwhile, LookAhead introduces a set of “slow weights”, which are updated based on the previous weight updates of the normal optimizer (RADam). The combination of both methods is highly synergistic, resulting in improved results. We train the model for 10 epochs because we now have $4x$ the data compared to training only the front camera images on a 24GB Titan RTX with a batch size of 20. We use a learning rate of $4 \times 10^{-4}$, which we reduce to $10^{-5}$ after 7 epochs for another 3 epochs. The distance decoder’s sigmoid output $\sigma$ is converted to distance using $D = m \cdot \sigma + n$. Depth is calculated for the pinhole model as $D = 1/(m \cdot \sigma + n)$, where $n$ and $m$ are constants chosen such that $D$ is constrained between 0.1 and 100. As described in Section IV-A (also cf. Fig. 3), we shuffle all images from the surround-view cameras with diverse viewpoints and present them to the distance and pose models along with their corresponding intrinsics to build the camera geometry tensor $C_t$. We limited the length of the sequences to three. The lengths of the sequences considered for pose estimation results are 2, 3, and 5. The semantic segmentation is trained supervised by applying the cross-entropy loss and optimized jointly with the distance estimation (see Fig. 2).

**Comparison to Convolutional Networks** Pairwise models match or outperform convolutional baselines while requiring comparable or lower parameters and FLOP budgets. In terms of computational complexity, the pairwise models outperform CNN’s. For example, the pairwise SAN10 with 11.8M params and 1.9G FLOPS outperforms ResNet50 with 25.6M params and 4.1G FLOPS, while having a $54\%$ lower parameter and $44\%$ lower FLOP count. SAN10-patch models’ parameter count is almost equivalent to ResNet18 with 11.7M params and 1.8G FLOPS, whereas SAN15-patch with 20.5M params and 3.3G FLOPS is equivalent to ResNet50’s parameter count. The SAN10-pairwise with 10.5M params and 2.2G FLOPS...
Fig. 4: **Distance estimation results** of the same network evaluated on four different fisheye cameras of a surround-view camera system. One can see that our SVDistNet model generalizes well across different viewing angles and consistently produces high-quality distance outputs.

| Method                        | Seg | Dist. | MTL (Synergy) | Seg. (mIOU) | Distance (RMSE) |
|-------------------------------|-----|-------|---------------|-------------|-----------------|
| SynDistNet [11]               | ✓   | ✓     | ✓             | 76.8        | ✓               |
|                               | ✓   | ✓     | ✓             | 2.316       |                 |
|                               | ✓   | ✓     | ✓             | 78.3        | 2.128           |
|                               | ✓   | ✓     | ✓             | 81.5        | 1.714           |
| SVDistNet (SAN10-patch)       | ✓   | ✓     | ✓             | 77.1        | ✓               |
|                               | ✓   | ✓     | ✓             | 2.153       |                 |
|                               | ✓   | ✓     | ✓             | 78.6        | 1.861           |
|                               | ✓   | ✓     | ✓             | 82.3        | 1.532           |

**TABLE I:** **Effect of our multi-task training approach** on semantic segmentation and distance estimation when using a ResNet 18 backbone for SynDistNet [11] and self-attention network SAN-10 for SVDistNet. We observe that both outputs improve through the multi-task training and mainly the distance estimation performance profits from the synergized semantic guidance.

outperforms ResNet18 with a 9% lower parameter count and 22% higher FLOP count. By performing a single-scale image depth prediction rather than the multi-scale in our previous works [9], [10], we could leverage the use of a more robust loss function over $L_1$ to reduce training times on SAN10.

VI. EXPERIMENTAL EVALUATION

A. Effect of Multi-Task Learning

In Table I, we compare our SVDistnet with previous work [11] on the Woodscape dataset [3]. Specifically, we evaluate our model using the pairwise self-attention encoder. First, we create single-task baselines using the various methods mentioned above, and then we create an important shared encoder-based multi-task learning (MTL) baseline for these tasks. Due to the use of an improved self-attention encoder and the camera geometry tensor, the MTL results and single-task benchmark for distance estimation outperform SynDistNet [11]. However, we observe only minimal gain for the semantic segmentation task. In the final experiment, we include the synergy between the distance and segmentation decoders. For these diverse tasks, we observe that the content and channel adaptive self-attention encoder features can be learned jointly, wherein the captured semantic features, used along with pixel-adaptive convolutions, guide the distance decoder to capture better geometric features. We use ablation experiments to further dissect these findings.

B. Ablation Study on the Single Contributions

For our ablation analysis, we consider two self-attention encoder variants: pairwise and patchwise. Table II displays the distance estimation results for these variants. We show the impact of certain contributions and their importance in our SVDistNet framework compared to our previous work SynDistNet [11]. As a start, we replace the $L_1$ loss with the general robust loss function and test it on the self-attention encoder’s patchwise variant, which results in significant accuracy improvements. To filter all the dynamic objects that contaminate the reconstruction loss, we use the dynamic object mask obtained by projecting semantic segmentation predictions as described in Section III-B. Furthermore, this contribution has the potential to solve the infinite distance problem.

We see a significant increase in accuracy after adding the camera geometry tensor to this setting. The training on multiple cameras with varying intrinsics and viewing angles adds an additional regularization. The network’s aforementioned training strategy is thereby more camera-independent and leads to a better generalization to images captured with varying cameras. To improve our multi-task setup even further, we use a distance and segmentation decoder synergy. We apply semantic features from the supervised task to the distance decoder’s geometric features while still training the distance
We use a higher-convolution, while the pairwise self-attention module equals encoder. The patchwise self-attention module outperforms the same level of accuracy as the patchwise self-attention encoder head. We were unable to achieve work. We also performed a few vital evaluations using the pair-our SVDistNet model for the surround view-camera frame-

## TABLE II: Ablation study on the effect of our contributions

| Network                  | RL | Self-Attn | SEM | Mask | CGT | Abs Rel | Sq Rel | RMSE | RMSE$_{log}$ | δ < 1.25 | δ < 1.25$^2$ | δ < 1.25$^3$ |
|--------------------------|----|-----------|-----|------|-----|---------|--------|------|--------------|----------|--------------|--------------|
| SinDistNet (ResNet18) [11] | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.128 | 0.469 | 2.153 | 0.164 | 0.875 | 0.974 | 0.986 |
| SinDistNet (ResNet50) [11] | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.110 | 0.381 | 1.856 | 0.135 | 0.884 | 0.985 | 0.994 |
| SVDistNet (SAN10-patch)   | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.094 | 0.345 | 1.789 | 0.128 | 0.887 | 0.985 | 0.992 |
| SVDistNet (SAN10-pair)    | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.074 | 0.343 | 1.641 | 0.112 | 0.892 | 0.985 | 0.994 |
| SVDistNet (SAN19-patch)   | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.092 | 0.378 | 1.861 | 0.133 | 0.884 | 0.984 | 0.991 |
| SVDistNet (SAN19-pair)    | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.089 | 0.351 | 1.773 | 0.129 | 0.886 | 0.986 | 0.993 |

By introducing our camera geometry tensor, we completed our SVDistNet model for the surround view-camera framework. We also performed a few vital evaluations using the pair-wise self-attention encoder head. We were able to achieve the same level of accuracy as the patchwise self-attention encoder. The patchwise self-attention module outperforms convolution, while the pairwise self-attention module equals or outperforms the convolutional equivalents. We use a higher-

## TABLE III: Ablation study on multiple cameras

| Cams | RL | Self-Attn | SEM | Mask | CGT | Abs Rel | Sq Rel | RMSE | RMSE$_{log}$ | δ < 1.25 | δ < 1.25$^2$ | δ < 1.25$^3$ |
|------|----|-----------|-----|------|-----|---------|--------|------|--------------|----------|--------------|--------------|
| Front | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.074 | 0.331 | 1.624 | 0.101 | 0.891 | 0.986 | 0.994 |
| Rear  | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.082 | 0.316 | 1.682 | 0.119 | 0.890 | 0.987 | 0.993 |
| Left  | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.067 | 0.296 | 1.578 | 0.106 | 0.895 | 0.985 | 0.994 |
| Right | ✔️ | ✔️ | ✔️ | ✔️ | ✔️ | 0.115 | 0.413 | 2.028 | 0.148 | 0.876 | 0.983 | 0.992 |

 estimation in a self-supervised manner. In this case, we can remove the dynamic object mask and still see improvements.

By adding the camera geometry tensor to this setting, we outperform all previous works on the Woodscape dataset [3]. From our distance estimation baseline [9], we incrementally add up the robust loss (RL), self-attention layers encoder heads (Self-Attn), semantic guidance in the decoder (SEM), dynamic object masking (Mask), and camera geometry tensor (CGT). We showcase our improvements for various network architectures and, in particular, show the superiority of our SVDistNet model over the SynDistNet model as well as the positive effect of using camera geometry tensor $C_t$. 

## C. Generalization Across Different Cameras

The generalization across different cameras from the surround-view setup is depicted in Table III using the camera geometry tensor as described in Section IV-A. Each camera's
For example, the front camera’s distance estimates profit as it aids in generalization during the model’s training phase. The method [7], in which the model is trained during inference, significantly improves the KITTI labels for depth estimation, we show a significant improvement. Simultaneously, our network architecture’s refinements, textit{we outperform all previous methods.}

**TABLE IV: Evaluation of the KITTI Eigen split in comparison to other self-supervised monocular depth estimation methods.** We limit depths to 80m in accordance with best practices. We also evaluate using the Original depth maps generated from raw point clouds as proposed by [46] and Improved annotated depth maps as introduced by [48]. M indicates that sequences are trained on using the monocular approach. The method” indicates the online refinement technique [7], in which the model is trained during inference.

D. State-of-the-Art Comparison on KITTI

To facilitate comparisons with previous methods, we also train our distance estimation method on the KITTI Eigen split [49], [46] in the classical depth estimation setting. First, we train and evaluate on depth maps generated from LiDAR point clouds, where Table IV shows that with our contributions, textit{we outperform all previous methods.}

We obtain a significant improvement using the online refinement method from [7], and our results remain superior to previous methods. Also, when training and evaluating the improved KITTI labels for depth estimation, we show a significant improvement. Simultaneously, our network architecture’s complexity is still comparable to the one of a ResNet18 in terms of computational complexity. We also use the general camera tensor $C_t$ as described in Section IV-A in our model, wherein instead of the angle of incidence maps, we employ the maps generated using Eq. 11 for pinhole cameras.

VII. CONCLUSION

In this paper, we solved the problem of multi-camera distance estimation for surround-view fisheye cameras. We introduced a novel camera model adaptation mechanism wherein camera parameters are transformed into a tensor and used within the CNN model. The specific camera model parameters are used during training and inference. Using this technique, we demonstrate training of a single distance estimation model for twelve different cameras with different extrinsic and intrinsic parameters and achieve the improved results as training a specialized model for each camera variant. We achieve state-of-the-art results on the fisheye WoodScape dataset and the KITTI dataset. We intend to learn and refine camera parameters’ within the training framework in future work.

REFERENCES

[1] M. Heimberger, J. Horgan, C. Hughes, J. McDonald, and S. Yogamani, “Computer vision in automated parking systems: Design, implementation and challenges,” in Image and Vision Computing. Elsevier, 2017.

[2] V. Ravi Kumar, S. Milz, C. Witt, M. Simon, K. Amende, J. Petzold, S. Yogamani, and T. Pech, “Monocular fisheye camera depth estimation using sparse lidar supervision,” in ITSC, 2018.

[3] S. Yogamani, C. Hughes, J. Horgan, G. Sistu, P. Varley et al., “Woodscape: A Multi-Task, Multi-Camera Fisheye Dataset for Autonomous Driving,” in ICCV, 2019.

[4] T. Zhou, M. Brown, N. Snavely, and D. G. Lowe, “Unsupervised learning of depth and ego-motion from video,” in CVPR, 2017.

[5] C. Godard, O. Mac Aodha, M. Firman, and G. J. Brostow, “Digging Into Self-Supervised Monocular Depth Estimation,” in ICCV, 2019.

[6] V. Ravi Kumar, S. Yogamani, S. Milz, and P. Maeder, “FisheyeDistanceNet++: Self-Supervised Fisheye Distance Estimation with Self-Attention, Robust Loss Function and Camera View Generalization,” in Electronic Imaging. Society for Imaging Science and Technology, 2021.

[7] V. Casser, S. Pirk, R. Mahjourian, and A. Angelova, “Depth Prediction Without the Sensors: Leveraging Structure for Unsupervised Learning from Monocular Videos,” in AAAI, 2019.

[8] M. Klingner, J.-A. Termöhlen, J. Mikolajczyk, and T. Fingscheidt, “Self-Supervised Monocular Depth Estimation: Solving the Dynamic Object Problem by Semantic Guidance,” in ECCV, 2020.

[9] V. Ravi Kumar, S. A. Hiremath, M. Bach, S. Milz, C. Witt et al., “FisheyeDistanceNet: Self-supervised scale-awire distance estimation using monocular fisheye camera for autonomous driving,” in ICRA, 2020.

[10] V. Ravi Kumar, S. Yogamani, M. Bach, C. Witt, S. Milz et al., “UnRectDepthNet: Self-Supervised Monocular Depth Estimation using a Generic Framework for Handling Common Camera Distortion Models,” in IROS, 2020.

[11] V. Ravi Kumar, M. Klingner, S. Yogamani, S. Milz, T. Fingscheidt et al., “SynDistNet: Self-Supervised Monocular Fisheye Camera Distance Estimation Synergized with Semantic Segmentation for Autonomous Driving,” in WACV, 2021.

[12] C. Godard, O. Mac Aodha, and G. J. Brostow, “Unsupervised Monocular Depth Estimation With Left-Right Consistency,” in CVPR, 2017.

[13] V. Guizilini, R. Ambrus, S. Pillai, and A. Gaidon, “3D Packing for Self-Supervised Monocular Depth Estimation,” in CVPR, 2020.

[14] F. Tosi, F. Alottti, M. Poggi, and S. Mattoccia, “Learning Monocular Depth Estimation Infusing Traditional Stereo Knowledge,” in CVPR, 2019.

[15] R. Wang, S. M. Pizer, and J.-M. Frahm, “Recurrent Neural Network for (Un-)Supervised Learning of Monocular Video Visual Odometry and Depth,” in CVPR, 2019.

[16] L. Zhang, C. Shen, Y. Li, Y. Cao, Y. Liu et al., “Exploiting Temporal Consistency for Real-Time Video Depth Estimation,” in ICCV, 2019.

[17] V. Casser, S. Pirk, R. Mahjourian, and A. Angelova, “Unsupervised Monocular Depth and Ego-Motion Learning With Structure and Semantics,” in CVPR-Workshops, 2019.

[18] A. Kendall, Y. Gal, and R. Cipolla, “Multi-Task Learning Using Uncertainty to Weigh Losses for Scene Geometry and Semantics,” in CVPR, 2018.

[19] L. Wang, J. Zhang, O. Wang, Z. Lin, and H. Lu, “SDC-Depth: Semantic Divide-and-Conquer Network for Monocular Depth Estimation,” in CVPR, 2020.

[20] M. Klingner, A. Bär, and T. Fingscheidt, “Improved Noise and Attack Robustness for Semantic Segmentation by Using Multi-Task Training with Self-Supervised Depth Estimation,” in CVPR-Workshops, 2020.

[21] M. Klingner and T. Fingscheidt, “Online Performance Prediction of Perception DNNs by Multi-Task Learning with Depth Estimation,” in IEEE Transactions on Intelligent Transportation Systems, 2021.
[22] S. Zhao, H. Fu, M. Gong, and D. Tao, “Geometry-Aware Symmetric Domain Adaptation for Monocular Depth Estimation,” in CVPR, 2019.

[23] P. Liu, M. Lyu, I. King, and J. Xu, “SelfFlow: Self-Supervised Learning of Optical Flow,” in CVPR, 2019.

[24] L. Liu, G. Zhai, W. Ye, and Y. Liu, “Unsupervised Learning of Scene Flow Estimation Fusing With Local Rigidity,” in IJCAI, 2019.

[25] Y. Chen, C. Schmid, and C. Sinno-Jeong, “Self-Supervised Learning With Geometric Constraints in Monocular Video Connecting Flow, Depth, and Camera,” in ICCV, 2019.

[26] V. Nekrasov, T. Dharmasiri, A. Spek, T. Drummond, C. Shen et al., “Real-time joint semantic segmentation and depth prediction using asymmetric annotations,” in IJCAI, 2019.

[27] V.-C. Mielec and S. Nedevschi, “Real-time semantic segmentation-based stereo reconstruction,” in IEEE Transactions on Intelligent Transportation Systems, 2019.

[28] V. Guizilini, R. Hou, J. Li, R. Ambrus, and A. Gaidon, “Semantically-Guided Representation Learning for Self-Supervised Monocular Depth,” in ICLR, 2020.

[29] P.-Y. Chen, A. H. Liu, Y.-C. Liu, and Y.-C. F. Wang, “Towards Scene Understanding: Unsupervised Monocular Depth Estimation With Semantic-Aware Representation,” in CVPR, 2019.

[30] S. Zhu, G. Brazil, and X. Liu, “The Edge of Depth: Explicit Constraints between Segmentation and Depth,” in CVPR, 2020.

[31] G. Yang, H. Zhao, J. Shi, Z. Deng, and J. Jia, “SegStereo: Exploiting Semantic Information for Disparity Estimation,” in ECCV, 2018.

[32] A. Gordon, H. Li, R. Jonschkowski, and A. Angelova, “Depth from Videos in the Wild: Unsupervised Monocular Depth Learning from Unknown Cameras,” in ICCV, 2019.

[33] J. M. Facil, B. Unmehothfer, H. Zhou, L. Montesano, T. Brox et al., “CAM-Conv: Camera-Aware Multi-Scale Convolutions for Single-View Depth,” in CVPR, 2019.

[34] F.-E. Wang, Y.-H. Yeh, M. Sun, W.-C. Chiu, and Y.-H. Tsai, “BiFuse: Monocular 360° Depth Estimation via Bi-Projection Fusion,” in CVPR, 2020.

[35] L. Jin, Y. Xu, J. Zheng, J. Zhang, R. Tang et al., “Geometric Structure Based and Regularized Depth Estimation From 360° Indoor Imagery,” in CVPR, 2020.

[36] J. T. Barron, “A General and Adaptive Robust Loss Function,” in CVPR, 2019.

[37] H. Zhao, J. Jia, and V. Koltun, “Exploring self-attention for image recognition,” in CVPR, 2020.

[38] J. P. Barreto, “Unifying image plane liftings for central catadioptric and dioptric cameras,” in Imaging Beyond the Pinhole Camera. Springer, 2006.

[39] B. Khomutenko, G. Garcia, and P. Martinet, “An Enhanced Unified Camera Model,” in RA-L, 2016.

[40] V. Usenko, N. Demmel, and D. Cremers, “The double sphere camera model,” in 3DV, 2018.

[41] R. Liu, J. Lehman, P. Molino, F. P. Such, E. Frank et al., “An Intriguing Failure of Convolutional Neural Networks and the CoordConv solution,” in NIPS, 2018.

[42] H. Su, V. Jampani, D. Sun, O. Gallo, E. Learned-Miller et al., “Pixel-Adaptive Convolutional Neural Networks,” in CVPR, 2019.

[43] L. Liu, H. Jiang, P. He, W. Chen, X. Liu, J. Gao, and J. Han, “On the variance of the adaptive learning rate and beyond,” in ICLR, 2020.

[44] M. Zhang, J. Lucas, J. Ba, and G. E. Hinton, “Lookout Optimizer: k steps forward, 1 step back,” in NIPS, 2019.

[45] D. P. Kingma and J. Ba, “Adam: A method for stochastic optimization,” in arXiv preprint arXiv:1412.6980, 2014.

[46] D. Eigen, C. Puhrsch, and R. Fergus, “Depth Map Prediction from a Single Image Using a Multi-Scale Deep Network,” in NIPS, 2014.

[47] C. Sha, K. Yu, Z. Duan, and K. Yang, “Feature-metric Loss for Self-Supervised Learning of Depth and Egomotion,” in ECCV, 2020.

[48] J. Uhrig, N. Schneider, L. Schneider, U. Franke, T. Brox et al., “Sparsity Invariant CNNs,” in 3DV, 2017.

[49] A. Geiger, P. Lenz, C. Stiller, and R. Urtasun, “Vision Meets Robotics: The KITTI Dataset,” in The Int. Journal of Robotics Research, 2013.

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