OBSERVATIONS OF MKN 421 WITH THE MAGIC TELESCOPE

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ABSTRACT

The MAGIC telescope took data of very high energy γ-ray emission from the blazar Markarian 421 (Mkn 421) between November 2004 and April 2005. We present a combined analysis of data samples recorded under different observational conditions, down to γ-ray energies of 100 GeV. The flux was found to vary between 0.5 – 2 Crab units (integrated above 200 GeV), considered a low state when compared to known data. Although the flux varied on a day-by-day basis, no short-term variability was observed, although there is some indication that not all nights are in an equally quiescent state. The results at higher energies were found to be consistent with previous observations. A clear correlation is observed between γ-rays and X-rays fluxes, whereas no significant correlation between γ-rays and optical data is seen. The spectral energy distribution between 100 GeV and 3 TeV shows a clear deviation from a power law, more clearly at lower flux than previous observations. The γ-ray emission from this blazar.

Subject headings: gamma rays, observations: BL Lacertae objects: individual (Mkn 421)

1. INTRODUCTION

Mkn 421 (redshift z = 0.030) is the closest known and, along with Mkn 501, the best studied TeV γ-ray emitting blazar. It was the first extragalactic source detected in the TeV energy range using imaging atmospheric Cherenkov telescopes (IACTs) (Punch et al. 1992; Petry et al. 1996). Mkn 421 is currently the source with the fastest observed flux variations among TeV γ-ray emitters. So far it has shown flux variations larger than one order of magnitude, and occasional flux doubling times as short as 15 min (Gaidos et al. 1996; Aharonian et al. 2002). Variations in the hardness of the TeV γ-ray spectrum during flares were reported by several groups (e.g. Krennrich et al. 2002; Aharonian et al. 2004). Simultaneous observations in the X-ray and GeV-TeV bands show strong evidence for flux correlation (Krawczynski et al. 2001; Blażejowski et al. 2002).
Mkn 421 has been detected and studied in all accessible wavelengths of the electromagnetic spectrum from radio waves to very high energy (VHE) γ-rays. The overall spectral energy distribution (SED) shows a typical two bump structure with the first peak in the keV energy range and the second maximum at GeV-TeV energies. The SED is commonly interpreted as beamed, non-thermal emission of synchrotron and inverse-Compton radiation from ultrarelativistic electrons, accelerated by shocks moving along the jets at relativistic bulk speed. Simple one-zone synchrotron-self-Compton (SSC) models (e.g. Coppi (1992); Costamante & Ghisellini (2002)) describe the observational results satisfactorily well. However, hadronic models (Mannheim et al. 1996; Mücke et al. 2003) can explain the observed features, too. A way to distinguish between the different emission models is to determine the position of the second peak in the SED, using simultaneous time-resolved data over a broad energy range through multiwavelength campaigns. This requires providing data in the as yet unexplored gap in the SED.

The MAGIC telescope (Major Atmospheric Gamma Imaging Cherenkov telescope; see Lorenz (2004)), located on the Canary Island La Palma (2200 m asl, 28°45′N, 17°54′W), completed its commissioning phase in early fall 2004. MAGIC is currently the largest IACT, with a 17 m diameter tesselated reflector dish consisting of 964 0.5 × 0.5 m² diamond-milled aluminium mirrors. Together with the current configuration of the MAGIC camera with the trigger region of 2.0 degrees diameter (Cortina et al. 2005), this results in a trigger collection area for γ-rays of the order of 10⁵ m², increasing with the zenith angle of the observation. Presently the accessible trigger energy range spans from 50-60 GeV (at small zenith angles) up to tens of TeV. The MAGIC telescope is focused to 10 km distance – the most likely position for a 50 GeV air shower. The accuracy in reconstructing the direction of incoming γ-rays on an event by event basis, hereafter γ-point spread function (PSF), is about 0.1 degrees, slightly depending on the analysis.

The first physics observations in winter 2004/05 and in spring 2005 included observations of the well-established TeV blazar Mkn 421. In total, 19 nights of data were taken on this source, the observation times per night ranging from 30 minutes up to 4 hours. Here we present the results from these observations, covering the energy range from 100 GeV to several TeV. We first describe the data set and analysis techniques in section 2. In section 3 we present the results and, finally, in section 4 we compare our results with other observations and interpret them in terms of different models.

2. OBSERVATIONS AND DATA ANALYSIS

The Mkn 421 data were taken between November 2004 and April 2005, and divided into four samples, for reasons given below. Data taken before and after February 2005 were treated separately, due to changes in the telescope hardware. Most of the data were taken at small zenith angles (ZA < 30°), i.e. at a low trigger energy threshold. However, observations made during 1.5 hours in a common campaign with the H.E.S.S. telescope system (Mazin et al. 2003) in December 2004 were taken at 42° < ZA < 55°. There were also different observational modes: the standard mode for MAGIC is the ON-OFF mode, with equal time given to tracking the source in the center of the camera (ON), and tracking a sky region near the source but with the source outside the field of view (OFF). This provides a robust estimate of the background. In our observations, we considered the γ-ray signal from Mkn 421 to be strong enough to obviate OFF observations, and we estimated the background level from the ON data (see below). In April 2005, part of the data were taken in the wobble mode (Daum et al. 1997). In this mode, two sky directions, opposite and 0.4° off the source, were tracked alternately for 20 minutes each, which provides a simultaneous measurement of signal and background. In the wobble mode there is a priori no need for additional OFF data.

The observation criteria and some important parameters of the four data samples are summarized in Table 1. For each data sample a separate Monte-Carlo (MC) set of γ events was simulated (CORSIKA version 6.023, Knapp & Heck (2004); Majumdar et al. (2005)), taking into account the zenith angle of observation, the observational mode, and the hardware setup of the telescope. The full data set corresponds to 29.0 hours ON-source observation time. Runs with problems in the hardware or with unusual trigger rates were rejected in order to ensure a stable performance and good atmospheric conditions. After removing these runs, the remaining observation time was 25.6 h.

For calibration, image cleaning, cut optimization, and energy reconstruction the standard analysis techniques of the MAGIC telescope (Bretz 2005; Wagner et al. 2005; Gaug et al. 2003) were applied as shortly described below. The calibration of the raw data from the MAGIC camera uses a system consisting of fast and powerful LED pulzers emitting at three different wavelengths with variable light intensity. Absolute calibration is obtained by comparing the signal of the pixels with the one obtained from a carefully calibrated PIN diode, and is cross-
TABLE 1
Results of the Mkn 421 data using the Alpha approach (see text for details). Samples I+II were recorded in November 2004 - January 2005, while samples III+IV were taken in April 2005.

| sample | on time | ZA range [°] | mode | $E_{\text{thr}}$ [GeV] | $N_{\text{on}}$ | $N_{\text{off}}$ | $N_{\text{excess}}$ | sigma |
|--------|---------|--------------|------|------------------------|--------------|-------------|----------------|------|
| I      | 4.63 h  | 9.3 - 31.2   | ON   | 150                    | 3761         | 1878 ± 32   | 1883 ± 69     | 29.3 |
| H      | 1.53 h  | 42.4 - 55.0  | ON   | 260                    | 1086         | 674 ± 25    | 413 ± 41       | 10.1 |
| III    | 9.30 h  | 9.2 - 27.5   | ON   | 150                    | 8083         | 4360 ± 49   | 3723 ± 102    | 38.9 |
| IV     | 10.12 h | 9.4 - 32.4   | wobble | 150       | 7740         | 4532 ± 67   | 3208 ± 111    | 29.1 |

checked by analysing muon rings. The time resolution of the read-out system has been measured to be about 700 ps for Cherenkov light flashes of 10 photo-electrons (ph.el.) per pixel, reaching 200 ps at 100 ph.el. Calibration events are taken at 50 Hz, interlaced with normal data, using an external calibration trigger.

The calibrated images are cleaned using so-called tail cuts: pixels are retained only if their reconstructed charge signals are larger than 10 ph.el. (‘core pixels’) or if their charges are larger than 5 ph. el. and they have at least one neighboring core pixel. The camera images are then reduced to image parameters as in (Hillas 1985), adding parameters describing the intensity concentration and asymmetry.

For $\gamma$/hadron separation a multidimensional classification technique based on the Random Forest (RF) method (Breiman 2001; Bock et al. 2004) was used. The RF method uses training data (randomly chosen data events and Monte Carlo $\gamma$s, representing background and signal) to find a set of classification trees in the space of image parameters. Multiple trees are combined to form a generalized predictor by taking the mean classification from all trees. The predictor, called hadronness, spans a range between 0 and 1, and characterizes the event images being less or more hadron-like.

In our analysis, classical image shape parameters like $\text{Width}$, $\text{Length}$, $\text{Dist}$ and $\text{Size}$ were used as input parameters. The cuts in hadronness for the $\gamma$/hadron sepa-
ration were trained for each data set separately, and were then chosen such that the overall cut efficiency for MC $\gamma$ events remained about 50%. The corresponding hadron suppression is about 90-99%, improving with increasing Size of the events.

A critical variable not used in the RF classification tree is Alpha, the angle between the major image axis and the line connecting the center of gravity of the image with the source position in the camera plane. In stand-alone IACTs, Alpha is commonly used, after all previously noted cuts, to extract the $\gamma$ signal from the data, and to estimate the level of background. For a point source, the Alpha distribution of the $\gamma$-like events is expected to peak at low values of Alpha, whereas for background events the distribution should be flat or slowly varying with Alpha.

In the case of our ON-mode data, the background remaining after $\gamma$/hadron separation was estimated from the Alpha distribution by performing a second order polynomial fit (without linear term) in the range between $30^\circ$ and $90^\circ$ where no contribution from $\gamma$ events is expected (see Fig. 1). The signal was then determined as the number of observed events in the range $\text{Alpha} < \text{Alpha}_0$ exceeding the fit extrapolated to small Alpha, where $\text{Alpha}_0$ is energy dependent and has a typical value of $15^\circ$. The significance of an excess is then calculated according to Eq. 17 in [Li & Ma (1983)].

In the wobble mode, the ON (source) data are defined by calculating image parameters with respect to the source position, whereas OFF data are obtained from the same events but with image parameters calculated with respect to the position on the opposite side of the camera, the antisource position. In order to avoid an unwanted contribution from $\gamma$-events in the OFF sample and to guarantee the statistical independence between the ON and the OFF samples in the signal region, the following procedure is applied: events with $\text{Alpha}_{\text{source}} < \text{Alpha}_0$ (with $\text{Alpha}_{\text{source}}$ calculated with respect to the source position) are excluded from the OFF sample, and events with $\text{Alpha}_{\text{antisource}} < \text{Alpha}_0$ (with $\text{Alpha}_{\text{antisource}}$ calculated with respect to the antisource position) are excluded from the ON sample. This cut assures that the Alpha distributions for ON and OFF events are statistically independent for $\text{Alpha} < \text{Alpha}_0$. The Alpha approach was used to determine the excess events for all four data sets (Table 1).

As an alternative to this classical approach using Alpha, the so-called $\theta^2$ approach can be applied, an approach more common for the analysis of data from a system of IACTs like HEGRA or H.E.S.S. The angle $\theta$ denotes the angular distance between the expected source position and the reconstructed origin of the initial $\gamma$-ray. Since for a single IACT the angle $\theta$ can not be reconstructed directly, the so-called Disp method [Fomin et al. 1994; Lessard et al. 2001; Domingo-Santamaría et al. 2005] was used to determine the source position in the camera plane, using position-independent image shape parameters. The number of excess events is then determined as the difference between the $\theta^2$ distributions for the source and background, respectively, similar to the Alpha approach. The background-subtracted $\theta^2$ distribution for samples III and IV is shown in Fig. 2. The average background was estimated from the wobble data themselves, by excluding the sector of the camera affected by the presence of the strong source. The solid line in Fig. 2 indicates the expectation from MC-$\gamma$ events for a point source. Computing $\theta^2$ also permits to produce sky maps in which for every $\gamma$-ray candidate an origin in the sky is assigned (see Fig. 3). Note that our signal analysis relies on the Alpha approach throughout.

These conservative analysis methods are known to produce reliable results for energies above 100 GeV. The energy regime below 100 GeV will require additional studies, in particular concerning the background rejection. Thus, for our analyzed sample the Size parameter (total amount of light of the image and in first order proportional to the energy) was required to be above 150 photoelectrons.

The energy estimation was performed using again the Random Forest technique, based on the image parameters of a MC $\gamma$ sample. This sample is statistically independent of the one used for the training of the $\gamma$/hadron separation cuts. Prior to the training of the energy estimation, loose (high-acceptance) cuts in hadronness and Alpha were applied to avoid a possible bias caused by outlier $\gamma$ events.

The energy thresholds of the individual analyses (as given in Table 1) are defined as the peak in the differential energy distribution of the MC-$\gamma$ events after all cuts. Our analyses showed that we were able to extract excess events with energies $\sim$50 GeV lower than the corresponding peak value.

The spectrum of the number of excess events in bins of true energy is determined from the spectrum in the estimated energy by an unfolding procedure. This procedure corrects for the finite energy resolution and for biases in the energy estimation. The unfolding program package used in MAGIC allows unfolding with a variety of methods [Anykev et al. (1991)], which differ in the way regularization is implemented. Unfolding results are only accepted if the results from the different methods are consistent with each other and if some criteria are satisfied concerning the regularization strength, the size of the noise component and the $\chi^2$ value. The latter is a measure of the agreement between the expected “measured” spectrum from the unfolded spectrum and the actually measured spectrum. The unfolding result presented in this analysis was obtained with an iterative method, as described in [Bertero (1989)].

To demonstrate the quality of the applied analysis and the good agreement with previous measurements by other experiments, we show in Fig. 4 the differential energy spectrum of the Crab Nebula data (“standard candle” of VHE $\gamma$-ray astronomy). The data were taken in 2004 and 2005 with observation conditions and telescope performance similar to those of the Mkn 421 data. Additional publications describing details of the calibration methods and the data analysis are in preparation.

3. RESULTS

3.1. The signal

During the entire observation period, Mkn 421 was found to be in a low flux state compared with existing data (around 1 Crab unit for a flux integrated above 200 GeV), but resulting in a clear signal in all four data samples. Fig. 1 shows the Alpha distribution of the $\gamma$-
candidates of the combined samples I, II, and III with an energy threshold of \( \sim 150 \) GeV. An excess of about 7000 events was found, which, for the given background, corresponds to an excess of more than 49 standard deviations. The number of excess events and the significances for the individual samples are summarized in Table 1.

Fig. 3 shows a sky map produced with the Disp method using samples III and IV. The reconstructed source position from the sky map (Fig. 3, indicated by the black cross) is centered at RA=+11h04’19’’

3.2. The light curve

The integral fluxes above 200 GeV, averaged over each night of observation, are shown in the upper panels of Fig. 5. Significant variations of up to a factor of four overall and up to a factor two in between successive nights can be seen. Since sample II has an energy threshold of 260 GeV it is not shown on the light curve. The relatively high analysis energy threshold of 200 GeV applied for the light curve ensures that the results are independent of the actual trigger thresholds during each night. In the middle panels of Fig. 5 the corresponding flux in the X-ray band as observed by the All-Sky-Monitor (ASM\(^{23}\)) on-board the RXTE satellite is shown. In the lower panels of Fig. 5 the optical data taken by the KVA telescope\(^ {24}\) on La Palma are shown. Note that the contribution of the host galaxy (appr. 8.0 mJy) has been subtracted. While the X-ray data show a moderate variability within the observation period, the optical flux stays almost constant.

For the 6 nights in April (MJD 53465 to 53471), the light curve above 200 GeV is shown in Fig. 6 in bins of 10 minutes. We also added the background rates for each night in the same binning, in order to demonstrate that the small variations in the excess rates and the daily changes are not caused by detector effects or atmospheric transmission changes. The vertical lines indicate the time in each night at which the observation mode was changed from ON to Wobble. The mean integral flux per night in units of \(10^{-9}\) cm\(^{-2}\) s\(^{-1}\) and the quality of the fit constant are shown in the panels. The horizontal dashed line corresponds to the integral flux of the Crab Nebula above 200 GeV. Combining the findings from the intra-night light curves we conclude that we did not find significant short-term flux variability within individual nights, despite the high sensitivity of MAGIC for such a search. Some of the nights, however, are less compatible with a constant flux than others, which might be an indication of some activity, albeit unstructured and difficult to quantify. On the other hand, we observe significant day-to-day variation by up to a factor of two, and differences up to a factor of four in the full sample.

3.3. The energy spectrum

3.3.1. The measured spectrum

For the spectrum calculation, we combined the entire data set because the differences between the fluxes on individual nights are rather moderate (see Fig. 5). The resulting averaged differential energy spectrum is shown in Table 2 and in Fig. 7 by filled grey boxes. The energy spectra extend from around 100 GeV to several TeV. The last spectral point at 4.4 TeV is an 95% upper limit. The error bars shown are statistical only. Systematic errors are estimated to be 15% on the absolute energy scale, which correspond to 44% on the absolute flux level for a

\(^{23}\) http://heasarc.gsfc.nasa.gov/xte_weather/

\(^{24}\) http://tur3.tur.iac.es/
Fig. 6.—Light curve for 6 nights in 2006 April in 10 minutes binning. Upper panels: flux above 200 GeV. Mean rate $R$ in units of $(10^{-9} \text{ cm}^{-2} \text{s}^{-1})$ and the quality of the fit by a constant are shown in the panel. Lower panels: mean background rate $R_{bg}$ per minute after cuts. Note the rising background rate towards the end of each observation slot, related to the rising moon. $R_{bg}$ and the quality of the fit by a constant are shown. The vertical dotted lines indicate the time of the switchover from the ON observational mode to the Wobble mode. The dotted horizontal line indicates the Crab Nebula integral flux above 200 GeV as measured by MAGIC (Wagner et al. 2005).
photon index of 2.2. The systematic error on the slope is estimated to be 0.2. The attenuation of the VHE photons by intergalactic low energy photons and the determination of the intrinsic spectrum of Mkn 421 are discussed below.

3.3.2. $\gamma$-ray absorption by the EBL

The VHE photons from Mkn 421 cross ~400 million light years on their way to Earth. They interact with the low energy photons of the extragalactic background light (EBL, see Nikishov (1962); Gould & Schréder (1964); Stecker et al. (1992); Hauser & Dwek (2001)) consisting of redshifted star light of all epochs and reemission of a part of this light by dust in galaxies. The most common reaction channel between VHE $\gamma$-rays and the low energy photons of the EBL is pair production $\gamma_{\text{VHE}} + \gamma_{\text{EBL}} \rightarrow e^+ e^-$, a reaction which has its largest cross section when the center of mass energy is roughly 3.6 times larger than the threshold energy of 2m_e. The intrinsic (de-absorbed) photon spectrum, $dN/dE_i$, of a blazar located at redshift $z$ is given by:

$$dN/dE_i = dN/dE_{\text{obs}} \times \exp[-\tau(E, z)],$$

where $dN/dE_{\text{obs}}$ is the observed spectrum and $\tau(E, z)$ is the optical depth. The distance to Mkn 421 implies that the optical depth (e.g. Eq. 2 in Dwek & Krennrich (2003)) strongly depends on the shape and absolute photon density of the EBL between 1 and 30 $\mu$m wavelength. A rather complicated distortion of the intrinsic spectrum takes place above ~100 GeV. Although the calculation of the optical depth is straightforward, the spectral energy distribution of the EBL is uncertain. Direct measurements of the EBL are difficult because of the strong foreground emission consisting of reflected sunlight and thermal emission from zodiacal dust particles. Hence, many measurements lead to upper limits (Hauser et al. 1998; Dwek & Arendt 1998). Several measurements claimed a direct detection of the EBL, but some of them are controversial (Matsumoto et al. 2003; Finkbeiner et al. 2000). An alternative method to determine the EBL are fluctuation analyses of the measured radiation. Since a part of the EBL originates from discrete sources, fluctuations in the number of sources in an observer’s field of view will produce fluctuations in the measured background (Kashlinsky et al. 1996; Kashlinsky & Odenwald 2000). A third method is the galaxy number counting in the deep field surveys, which provides robust lower limits to the SED of the EBL (Elbaz et al. 2002; Metcalfe et al. 2003; Fazio et al. 2004; Madau & Pozzetti 2000). The results of these methods and measurements are summarized in Fig. 8.

In principle, upper limits on the EBL can also be determined from observed $\gamma$-ray spectra from medium to high redshift TeV blazars. Under assumptions that the reconstructed TeV blazar spectrum is not too hard and it does not have a pile-up at high energies, the EBL level can be constrained (see Hauser & Dwek 2001 for summary and Aharanion et al. 2004 for latest results). However, since the measured spectrum of Mkn 421 is much softer that the one of Mkn 501, which is located at similar redshift, the softness seems to be intrinsic. In addition, the data in this paper extend up to 3 TeV only (historical data of Mkn 421 extend up to 20 TeV), which further weakens possible constraints from such a nearby source. We therefore do not try to constrain EBL using this Mkn 421 data set.

Instead, we adopt the recent model of Primack et al. (2005), scaled up by a factor 1.5 (which is within the model uncertainties), to match lower limits set by the Spitzer mission and ISOCAM in the range of 4 to 15 $\mu$m (Fazio et al. 2004; Elbaz et al. 2002; Metcalfe et al. 2003). The resulting EBL spectrum is shown in Fig. 8 by the black curve. This EBL spectrum agrees with alternative models (e.g. Kneiske et al. 2004; Pei et al. 1999; Blain et al. 1999; Stecker et al. 2006) which are designed to predict the EBL today. It is also very close to the upper limits inferred from arguments on AGN spectra (Aharanion et al. 2006). Using this EBL spec-

![Fig. 7.](image-url) Differential energy distribution for Mkn 421 averaged over the whole data sample. The measured energy spectrum is shown by the grey full squares and the de-absorbed spectrum by the black full circles. The spectral point at the highest energy is a 95% upper limit. The grey shaded area corresponds to a systematic error from a slope error of ±0.2 as quoted in the text. The black solid line indicates the best fit to the de-absorbed spectrum by a power law with exponential cut-off; its parameters are listed in the inlay. For comparison reasons, the measured Crab Nebula spectrum (Wagner et al. 2005) is shown by the grey dotted line.

| energy bin [GeV] | lower limit mean energy upper limit bin limit | differential flux $dN/dE$ [photons/ (TeV cm$^2$ s)] |
|------------------|------------------------------------------|----------------------------------|
| 108              | 134                                      | 167                              | (3.72 ± 0.34) × 10$^{-9}$          |
| 167              | 208                                      | 259                              | (1.21 ± 0.04) × 10$^{-9}$          |
| 259              | 321                                      | 402                              | (3.77 ± 0.15) × 10$^{-10}$         |
| 402              | 498                                      | 623                              | (1.32 ± 0.05) × 10$^{-10}$         |
| 623              | 770                                      | 965                              | (3.63 ± 0.19) × 10$^{-11}$         |
| 965              | 1192                                     | 1497                             | (8.95 ± 0.71) × 10$^{-12}$         |
| 1497             | 1845                                     | 2321                             | (2.26 ± 0.27) × 10$^{-12}$         |
| 2321             | 2856                                     | 3598                             | (2.88 ± 1.20) × 10$^{-13}$         |
| 3598             | 4429                                     | 5579                             | < 1.10 × 10$^{-13}$               |
Energy density of the extragalactic background light (EBL). Direct measurements, galaxy counts, low and upper limits are shown by different symbols as described in the legend. The black solid curve is the EBL spectrum as in Primack et al. (2005) for z=0 but upscaled by a factor 1.5 to match low limits derived from the galaxy counts (Elbaz et al. 2002; Metcalfe et al. 2003; Fazio et al. 2004).

**TABLE 3**

| Systematic study of the fit parameters on the de-absorbed spectrum of Mkn 421. The fitted function is a power law with an exponential cut-off: 

\[
\frac{dN}{dE} = N_0 (E/	ext{0.2 TeV})^{-\alpha} \exp(-E/E_{\text{cut-off}}).
\]

We show fit values on the photon index, \(\alpha\), and the cut-off energy, \(E_{\text{cut-off}}\), for following assumptions: nominal values (A), a systematic shift by +18\% in the VHE energy scale (B), a systematic shift by -18\% in the VHE energy scale (C), a systematic shift by +18\% in the VHE energy scale and, in addition, 25\% more density of the EBL (D), and a systematic shift by -18\% in the VHE energy scale and, in addition, 25\% less density of the EBL (E). Note that the resulting systematic errors are comparable with the statistical errors.

| \(\alpha\) | \(E_{\text{cut-off}}\) (TeV) |
|---------|------------------|
| A: nominal | 2.20 ± 0.08 | 1.44 ± 0.28 |
| B: E+18\% | 2.16 ± 0.08 | 1.59 ± 0.29 |
| C: E-18\% | 2.24 ± 0.08 | 1.26 ± 0.26 |
| D: (E+18\%) + (EBL+25\%) | 2.12 ± 0.08 | 1.61 ± 0.29 |
| E: (E-18\%) + (EBL-25\%) | 2.20 ± 0.08 | 1.09 ± 0.20 |

3.3.3. The de-absorbed spectrum of Mkn 421
The measured spectrum and the reconstructed de-absorbed (i.e. corrected for the effect of intergalactic absorption) spectrum are shown in Fig. 7. For comparison reasons, the Crab Nebula spectrum is also shown. The de-absorbed spectrum (shown by filled black circles) is clearly curved, its probability of being a simple power law is $1.6 \times 10^{-8}$. The de-absorbed spectrum is fitted by a power law with an exponential cut-off: $dN/dE = N_0 (E/0.2\, \text{TeV})^{-\alpha} \exp(-E/E_{\text{cutoff}})$, $\alpha$ being the photon index, solid line in Fig. 7. The fit parameters are listed in the inlay of Fig. 7. The power law with a cut-off describes well the de-absorbed spectrum of Mkn 421, with a photon index $\alpha = 2.20 \pm 0.08$ and a cut-off energy of $E_{\text{cutoff}} = (1.44 \pm 0.28)\, \text{TeV}$. Taking into account the systematic uncertainty of 18% on the absolute energy scale of our measurement and in addition a guessed 25% uncertainty on the EBL level, we find that neither the photon index nor the cut-off energy substantially change (See Table 3). The fitted photon index was found to be between 2.12 and 2.24, whereas the cut-off energy was found to be between 1.1 and 1.6 TeV. From this study we conclude that the curvature of the spectrum is source inherent: either at the measured flux level this cosmic accelerator is close to its energy limit, or there exists a source–intrinsic absorption.

4. DISCUSSION

4.1. Comparison with previous observations of Mkn 421

In Fig. 10 we show the (de-absorbed) energy density spectrum in context with several previously published high statistics observations of Mkn 421. For a compilation of the VHE measurements of Mkn 421 we used historical data from CAT (Piron et al. 2001),
All results seem consistent with each other, and all show significant deviations from a simple power law, which can not be explained by attenuation effects (the results are robust with respect to the EBL model within a factor \( \pm 25\% \)). They are, therefore, likely to be source–intrinsic.

From the compilation of the de-absorbed Mkn 421 spectra, it is evident that with an increasing flux state the spectrum becomes harder. In order to verify this, we fitted the spectra by a simple power law \( (dN/dE \propto E^{-\alpha}) \) in the overlapping energy region between 700 GeV and 4 TeV. The resulting photon indices \( \alpha \) as function of the fitted flux at 1 TeV are shown in Fig. 11. Evidently, with increasing flux the spectra harden. Similar results were obtained using Whipple data (Krennrich et al. 2002), HEGRA data (Aharonian et al. 2002, 2003), and CAT data (Giebels et al. 2002).

The curvatures observed are indicative of a maximum in energy density, and are usually interpreted as due to inverse-Compton (IC) scattering. The peak position appears to be dependent on the source flux intensity. We have, therefore, performed a log-parabolic fit for all available data. The log-parabola has the following parametrization: 

\[
\log 10(\nu F_\nu) = A + B (\log 10(E) - \log 10(E_p)),
\]

with \( \nu F_\nu = E^2 dN/dE \) and \( E_p \) being the energy of the peak position. The best log-parabolic fits are shown in Fig. 10 by the dashed lines. In Fig. 12 we compare the resulting peak positions for the different experiments as a function of their (fitted) energy density at 1 TeV. Evidently, with increasing flux the peak shifts to higher energy values. Future observations at higher intensities extending to lower energies will have to corroborate these results. Such observations are part of the future MAGIC physics programme.

4.2. A short comment on the light curves

In the observation period between November 2004 and April 2005 we observed night-to-night flux variations up to a factor of 2 and a maximum flux change in the entire set of a factor 4. No short-term flux variations well below 1 hour, as observed during high flaring activity in previous experiments (Gaidos et al. 1996; Aharonian et al. 2002), were seen, although the sensitivity of MAGIC would allow to detect fast flares in the given flux range. Two equally likely explanations are that either we deal with large fluctuations resulting in the absence of any fast flare during the observation period, or fast flaring is a feature that occurs only when the source is very active. This calls for further high statistics and high sensitivity studies when the source is in its low flux state.

4.3. Correlation studies

The correlation between the \( \gamma \)-ray flux measured by MAGIC and the X-ray flux measured by RXTE/ASM is shown in Fig. 13. For the MAGIC flux we take the nightly average above 200 GeV (see also Fig. 5). For the X-ray data, we calculate the average of those RXTE/ASM pointings (dwell) which were taken simultaneously with MAGIC data, allowing \( \pm 1 \) hour with respect to the MAGIC data, to increase X-ray statistics. Fig. 13 shows a clear correlation between X-ray and \( \gamma \)-ray data. The linear fit (solid line), forced to go through \((0,0)\), has a slope of \( 1.4 \pm 0.1 \left( \frac{10^{-10}}{cm^2/s/TeV} \right) \), and has a \( \chi^2 \) probability of 54\%. The parabolic fit (dashed line) which

\[
\text{slope} = -0.027 \pm 0.002
\]

\[
\frac{\chi^2}{\text{ndf}} = 43.4 / 11
\]
Given the temporal correlation between X-ray and \( \gamma \)-ray fluxes, it is reasonable to infer that the VHE \( \gamma \)-ray radiation is dominated by emission resulting from IC upscattering of the synchrotron X-ray photons by their parent population of relativistic electrons. Such correlation can be modelled with a homogeneous synchrotron-self-Compton (SSC) model. Based on this model it is possible to constrain the parameter space of the emission region and estimate its basic parameters, the Doppler factor, \( D \), and the rest-frame magnetic field, \( B \), of the emitting plasma in the relativistic jet. To this end we follow the procedure first devised by Bednarek & Protheroe (1997) for the Mkn 421 flare of 16 May 1994, subsequently improved by, e.g., Tavecchio et al. (1998); Bednarek & Protheroe (1999); Kataoka et al. (1999); Katarzynski et al. (2003). Application of this method requires precise simultaneous multiwavelength information. Since a synchrotron (X-ray) spectrum simultaneous with the MAGIC observations is not available, we have to resort to previous X-ray observations arguing that similar TeV \( \gamma \)-ray states (IC emission) should correspond to similar X-ray states (synchrotron emission). In fact, similar \( \gamma \)-ray spectra of Mkn 421 have already been observed several times – including the HEGRA observations in April 1998 (Aharonian et al. 1999) for which simultaneous BeppoSAX observations are available (Fossati et al. 2000; Massaro et al. 2004). Here we use the X-ray spectra and parameterization, reported by Massaro et al. (2004) for 21 April 1998. It is also noticeable that the X-ray flux level between the simultaneous RXTE/ASM data and the BeppoSAX data used here is very similar (see Fig. 16).

The low flux state MAGIC \( \gamma \)-ray spectrum, reported here for energies at \( \sim 100 \) GeV, warrants a better investigation of the crucial energy range where the IC peak is expected to occur, than in previous data sets. Following Bednarek & Protheroe (1997, 1999) we then constrain the allowed parameters of the emission region \((D, B)\) from the ratio of the \( \gamma \)-ray power to the X-ray power, measured at their respective peak emission (see thick curves in the upper panels of Fig. 15). The radiation field density and the electron spectrum, cospatial in the blob, were derived as a function of \( D \) and \( B \) for a blob radius assumed equal to the light travel time scales (for observational arguments see Takahashi et al. 2000). We further constrain the allowed parameter space by arguing that the synchrotron and IC cooling time scales should be shorter than the observed variability time scale. These conditions are fulfilled above the dot-dashed lines (for synchrotron cooling) and on the left of the grey dashed line (for the IC cooling) for the 1 hr (upper left panel of Fig. 15) and 1 day (upper right panel of Fig. 15) variability time scales. The condition that the blob has to be transparent to the VHE \( \gamma \)-rays leads to a further lower bound on \( D \) by requiring that the optical depth by pair production has to be lower than unity. The corresponding limits for photon energies of 100 GeV and 3 TeV (which define the energy range of MAGIC measurement) are shown in the upper panels of Fig. 15 as thin and thick dotted lines, respectively. One last

**Fig. 13.—** Correlation between MAGIC integral flux measurements above 200 GeV and RXTE/ASM counts for 13 nights.

**Fig. 14.—** Correlation between MAGIC integral flux above 200 GeV and optical flux measured by the KVA telescope for 8 nights.
condition arises from comparing the maximum energy of electrons, determined by the maximum energy of synchrotron photons $\sim 40$ keV, with the maximum energy of the detected photons $\sim 3$ TeV (see dashed line in the upper panels of Fig. 15). These limiting conditions build an allowed region in the $D$-$B$ plane as marked by the grey shaded area. The allowed parameters of the emission region correspond to the part of the thick full curve inside the region limited by all these lines (see Fig. 15). In order to determine the values of $D$ and $B$ more precisely, we now calculate the $\gamma$-ray spectra for the points A, B, and C for 1 hr variability, and the points D, E, and F for 1 day variability, and compare the predicted spectrum with the actual de-absorbed spectrum. From the lower panels of Fig. 15 it is clear that the best description is provided by the blob with Doppler factor $D \sim 22$ and magnetic field $B \sim 0.7$ G (the point B) for 1 hr variability, and $D \sim 9$ and $B \sim 0.3$ G (the point D) for 1 day variability. In order to assess how this result is sensitive on the correct energy localization of the peak in the $\gamma$-ray spectrum (which is in fact only limited by the lower energy end of the MAGIC spectrum), we show the allowed parameter space for the $\gamma$-ray peak at 10 GeV (see thin full curves in Fig. 15). The constraints for the
Fig. 16.—The overall SED of Mkn 421 from optical wavelengths through VHE \( \gamma \)-rays. Large symbols represent averaged data described in this paper: optical data from KVA (star), X-rays from RXTE/ASM (full square), de-absorbed \( \gamma \)-rays from MAGIC (full points). The grey full squares are archival EGRET measurements (Hartman et al. 1999). The grey curve in the X-rays corresponds to the log-parabolic fit taken from Massaro et al. (2004) using BeppoSAX (Boella et al. 1997) data of Mkn 421 taken on 21 April 1998. The two black curves through the \( \gamma \)-ray spectrum (almost indistinguishable) correspond to the SSC model parameter sets B and D (see text and Fig. 15 for details). The grey dashed line denotes a fit by the SSC model as in Krawczynski et al. (2004), see text for details.

In Fig. 16 we show the broadband SED of Mkn 421. Large symbols represent averaged data described in this paper: optical data from KVA (star), X-rays from RXTE/ASM (full square), \( \gamma \)-rays from MAGIC (full points). The grey curve in the X-rays corresponds to a log-parabolic fit performed by Massaro et al. (2004) on BeppoSAX data of Mkn 421 taken on 21 April 1998. The two black curves through the \( \gamma \)-ray spectrum are almost indistinguishable and correspond to the best SSC model parameters for 1-hr and 1-day variability time scales (points B and D respectively, calculated according to Eq. (13) in Bednarek & Protheroe (1999) who apply the Klein-Nishina cross-section as in 2.48 of Blumenthal & Gould (1970)).

In addition, we apply the SSC code provided by Krawczynski et al. (2004) to our dataset. The fitted overall SED is shown by the grey dashed line in Fig. 16 and the model parameters are listed in Table 4. For the fit, we used the simultaneous KVA, ASM and MAGIC data, as well as the archival BeppoSAX observations from 21 April 1998 (Massaro et al. 2004). In contrast to the parameters adopted in Krawczynski et al. (2001), we used a smaller Doppler factor (15 instead of 50), resulting in a somewhat larger emitting region \( 1.6 \times 10^{16} \) cm instead of \( 2.7 \times 10^{15} \) cm), and a higher particle density \( 0.06 \) erg/cm\(^3\) instead of \( 0.01 \) erg/cm\(^3\). We note that the fitted values of magnetic field and Doppler factor are within the allowed range as defined above. Remarkably, the archival EGRET data (Hartman et al. 1999) matches the fit almost perfectly, suggesting an IC peak around 100 GeV.

### Table 4

| Parameter                | Value                  |
|--------------------------|------------------------|
| Doppler factor           | 15                     |
| Magnetic field           | 0.20 Gauss             |
| Radius of emitting region| \( 1.6 \times 10^{16} \) cm |
| Injected electron spectrum: | electronic energy density | \( 0.06 \) erg/cm\(^3\) |
|                         | \( 5 < \log_{10} (E [\text{eV}]) < 10.9 \) | index 2.31 |
|                         | \( 10.9 < \log_{10} (E [\text{eV}]) < 11.6 \) | index 3.88 |

5. CONCLUDING REMARKS

Mkn 421 was observed with the MAGIC telescope during several months in 2004 and 2005. Briefly, we have presented the following:

- first high-sensitivity observation down to \( \approx 100 \) GeV;
- first observation of an IC peak at low flux;
- absence of short flares below 1 hour duration despite sufficient sensitivity;
- flux variation up to a factor 2 between consecutive nights and up to a factor 4 in the entire observation period;
- confirmation of a source–inherent effect resulting in a curved spectrum after de-absorption (for reasonable assumptions concerning the EBL) in case of low flux intensity;
- a strong correlation between spectral hardness (photon index between \( 700 \) GeV and \( 4 \) TeV) and flux intensity, obtained by comparison of the de-absorbed energy spectra of various experiments covering different flux levels;
- a clear trend for the peak position to shift towards higher energies with increased source intensity, obtained by the same comparison;
- confirmation of a significant correlation between X-ray and VHE \( \gamma \)-ray intensity during a state of low to medium intensity;
- a hint that different flaring states result from differences in electron populations (electron spectrum) rather than from significant change of the blob’s Doppler factor and magnetic field strength.

We add the following conclusions. The flux state was found to be comparatively low, ranging in intensity between 0.5 and 2 Crab units when integrated above 200 GeV. While clear night to night variations were
found, the intra-night light curve, binned in 10-minute time intervals, does not show significant variations, although several nights are only marginally compatible with a constant flux. They do not show a discernible structure, though, and seem not associated to an overall flux different from that of perfectly quiescent nights. We note that MAGIC is sensitive enough to detect variabilities on the 10-minute time scale at such a low flux level. A clear correlation ($\gamma = 0.64^{+0.13}_{-0.09}$) between X-rays and $\gamma$-rays was found, while no correlation was seen between optical and $\gamma$-rays. This supports a leptonic origin of the $\gamma$-rays from Mrk 421. The energy spectrum resulting from the combined MAGIC data, corrected for the extragalactic absorption, suggests the presence of an IC peak at about 100 GeV. The spectrum is clearly curved at energies above 1 TeV, and can be fitted by a power-law with an exponential cut-off. The overall SED observed in the observed flux state can be well described by a homogeneous SSC model provided that the emission region moves with a Doppler factor $\sim 9$ and its magnetic field strength is $\sim 0.3$ G for a 1-day variability time scale. Surprisingly, these parameters do not differ substantially from those estimated for the emission region of Mrk 421 during a strong flare \cite{Bednarek97}. The fit with an alternative SSC code of Krawczynski et al \cite{Krawczynski01} lead to similar Doppler factor and magnetic field values.

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