Towards a 1% measurement of the Hubble Constant: accounting for time dilation in variable-star light curves

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ABSTRACT

Assessing the significance and implications of the recently established Hubble tension requires the comprehensive identification, quantification, and mitigation of uncertainties and/or biases affecting \( H_0 \) measurements. Here, we investigate the previously overlooked distance scale bias resulting from the interplay between redshift and Leavitt laws in an expanding Universe: Redshift–Leavitt bias (RLB). Redshift dilates oscillation periods of pulsating stars residing in supernova-host galaxies relative to periods of identical stars residing in nearby (anchor) galaxies. Multiplying dilated log \( P \) with Leavitt Law slopes leads to underestimated absolute magnitudes, overestimated distance moduli, and a systematic error on \( H_0 \). Emulating the SH0ES distance ladder, we estimate an associated \( H_0 \) bias of \((0.27 \pm 0.01)\%\) and obtain a corrected \( H_0 = 73.70 \pm 1.40 \text{ km s}^{-1} \text{ Mpc}^{-1}\). RLB becomes increasingly relevant as distance ladder calibrations pursue greater numbers of ever more distant galaxies hosting both Cepheids (or Miras) and type-Ia supernovae. The measured periods of oscillating stars can readily be corrected for heliocentric redshift (e.g. of their host galaxies) in order to ensure \( H_0 \) measurements free of RLB.

Key words. distance scale – Stars: oscillations – Stars: variables: Cepheids – Stars: variables: general – Stars: distances – Galaxies: distances and redshifts

1. Introduction

Pulsating stars such as classical Cepheids enable precise measurements of the local expansion rate of the Universe, \( H_0 \), thanks to the existence of period-luminosity relations (PLRs), or Leavitt laws (Leavitt 1908; Leavitt & Pickering 1912, henceforth: LLs). Using a Cepheid-based distance ladder, the SH0ES team (Riess et al. 2016, henceforth: R+16) recently established a systematic difference between the present-day value of \( H_0 \) and the value inferred based on Cosmic Microwave Background observations by the Planck Collaboration (2018) assuming the concordance cosmological model (flat ΛCDM). Following further improvements to the distance ladder (e.g. Riess et al. 2018, 2019), and considering Cepheid-independent routes to measure \( H_0 \) (e.g. Wong et al. 2019; Freedman et al. 2019; Yuan et al. 2019), the so-called Hubble tension now figures at a significance of \( 4 \sigma \), sparking an increasing number of suggested modifications to ΛCDM (for a detailed overview, see Verde et al. 2019, and references therein).

The SH0ES distance ladder consists of three rungs that are fitted globally (cf. Appendix in R+16). The first rung involves the calibration of the Cepheid LL in relatively nearby, so-called “anchor” galaxies whose distances are known. The second rung consists of so-called “SN-host” galaxies, where both Cepheids and type-Ia supernovae (SNe Ia) have been observed: SN-host galaxies thus set the luminosity zero-point for SNe Ia. The third, final rung consists of the Hubble diagram of SNe Ia. The intercept of this Hubble diagram provides the measurement of \( H_0 \). Almost all SN-host galaxies are more distant than the anchor galaxies, with the exception of M101, which is approximately 0.9 Mpc closer than the anchor galaxy NGC 4258. Following an improvement of the distance to NGC 4258, the latest \( H_0 = 73.5 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}\) (Reid et al. 2019).

Following impressive gains in \( H_0 \) precision and the importance of \( H_0 \) for informing modifications to ΛCDM, the identification and mitigation of previously overlooked \( H_0 \) uncertainties and biases is rapidly gaining importance. Notably, the effects of stellar association bias (Anderson & Riess 2018) are now taken into account in the \( H_0 \) measurement (Riess et al. 2019). A key bottleneck for increasing \( H_0 \) precision is the number of SN-host galaxies. At present, Cepheids can be measured with good precision in galaxies up to ~ 40 Mpc distant (R+16), and large efforts are in progress to increase the number of SN-host galaxies from currently 19 to 38 (Riess et al. 2019). However, the rather low volumetric rate of SNe Ia explosions requires exploring alternative primary distance indicators capable of probing greater distances, such as Mira-variable stars (e.g. Whitelock et al. 2008; Yuan et al. 2017; Huang et al. 2018, 2019; Bhardwaj et al. 2019), especially considering the short mission duration of the James Webb Space Telescope (JWST). Adding new SN-host galaxies to the distance ladder will therefore tend to include more distant galaxies and increase average SN-host galaxy redshift due to the Hubble-Lemaître law (Wirtz 1924; Lemaître 1927; Hubble 1929).

The longitudinal Doppler effect shifts the oscillation frequency emitted by a source as a function of its radial (line-of-sight) velocity, \( v_r \). Time dilation due to cosmological redshift \( z \) slows down clocks in a mathematically approximately identical way in the case of small \( z \) and non-

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relativistic velocities \((v_r \ll c)\). Thus, time dilation of the type Ia supernova SN 1995K enabled observational proof of the Universe’s expansion (Leibundgut et al. 1996). Several studies have considered the impact of inaccuracies related to redshift measurements of SNe Ia (e.g. Hui & Greene 2006; Davis et al. 2011, 2019) on \(H_0\) and the dark energy equation of state. Additionally, the impact of Doppler frequency shifts for asteroseismic inferences was studied by Davies et al. (2014) and is gaining importance for measuring orbital motion in pulsating stars (Murphy et al. 2014). However, the impact of systematic differences in (observed heliocentric) redshift between anchor and SN-host galaxies on variable-star periods and the \(H_0\) measurement has hitherto remained unexplored.

This article investigates the relevance and impact of dilated variable-star periods on the measurement of \(H_0\). Specifically, §2 explains the distance bias arising from cosmic expansion, the Doppler effect, and the Leavitt law in the case of Cepheids and Mira stars. §3 estimates the impact on the latest \(H_0\) measurement involving Cepheids and SNe Ia. §4 discusses these findings in the context of future distance ladders based on Mira-variable stars in the era of the JWST. Finally, §5 summarises this work and presents its conclusions.

2. Redshift-Leavitt Bias (RLB)

The observed total redshift of an extragalactic source relative to the observer is a combination of cosmological redshift \((\tilde{z})\), peculiar motion of the galaxy \((z_{\text{pec}}^{\text{gal}})\), peculiar motion of the observer \((z_{\text{pec}}^{\text{obs}})\), and gravitational redshift of the galaxy \((z_{\text{gal}}^{\text{obs}})\) and the observer \((z_0)\). Once corrected to the heliocentric reference frame, the observed redshift \(z_{\text{obs}}\) is

\[
1 + z_{\text{obs}} = (1 + \tilde{z})(1 + z_{\text{pec}}^{\text{gal}})(1 + z_{\text{pec}}^{\text{obs}})(1 + z_{\text{gal}}^{\text{obs}})(1 + z_0) . \tag{1}
\]

Variability periods of extragalactic variable stars such as classical Cepheids are subject to both time dilation due to cosmological redshift (mostly relevant for Cepheids outside the Local Group), and the Doppler effect due to line-of-sight motions such as peculiar velocities, velocity dispersions, partial sampling of a galaxy’s rotation curve, orbital motion, etc. Since the latter velocities are usually \(<1000\, \text{km}\,\text{s}^{-1}\), such Doppler shifts can be treated non-relativistically to very good approximation. The observed redshift of an individual variable star in another galaxy is thus:

\[
1 + z_{r,\text{obs}} \approx (1 + z_{\text{obs}}) \left(1 + \frac{v_{r,i}}{c}\right) , \tag{2}
\]

where \(v_{r,i}\) is the line-of-sight component of the star’s motion relative to the heliocentric reference frame, not counting peculiar motion, which is already included as part of Eq. 1. Of course, \(v_{r,i}\) of individual Cepheids is currently measurable only in the Milky Way and Magellanic Clouds, where cosmological redshift is negligible. For individual variable stars in other galaxies, internal motions due to velocity dispersion and partially sampled rotation curves can lead to \(v_{r,i}/c \lesssim 10^{-3}\). However, most observed populations of Cepheids in SN-host galaxies sample all parts of their host galaxy disks, which furthermore tend to be oriented relatively face-on. Hence, no significant net effect is to be expected for a typical SN-host galaxy’s Cepheid population as a whole, meaning, \(\langle v_r \rangle \approx 0\). For partially sampled galaxies (e.g. the PHAT footprint of M31, cf. Dalcanton et al. 2012), disk or halo rotation could lead to a net \(\langle v_r \rangle \lesssim \pm 300\, \text{km}\,\text{s}^{-1}\), which would be comparable to the effect of \(\tilde{z}\) at distances \(<4\, \text{Mpc}\).

Galaxy catalogs list redshifts \((z_{\text{obs}})\) measured as the displacement of spectral lines relative to their rest-wavelength \(\lambda_0\), corrected to the heliocentric reference frame (e.g. Huchra et al. 1992):

\[
z_{\text{obs}} = \frac{\lambda - \lambda_0}{\lambda_0} . \tag{3}
\]

\(z_{\text{obs}}\) does not distinguish between the physical origin of redshift, and includes all terms listed in Eq. 1. However, it does not account for motions of individual stars \((v_{r,i})\) or velocity differences across a galaxy. In the following, we neglect these latter two contributions since Cepheid populations are usually distributed across the full disks of SN-host galaxies, which are usually oriented face-on (R +16). However, observers may consider accounting for net effects, due to galaxy rotation at distances \(<40\, \text{Mpc}\), if these conditions are not fulfilled.

Using \(z_{\text{obs}}\), we calculated the effect of time dilation on variable-star periods (cf. Fig. 2) as

\[
P_{\text{obs}} = (1 + z_{\text{obs}})P_0 , \tag{4}
\]

\[
\Delta \log P = \log P_{\text{obs}} - \log P_0 = \log (1 + z_{\text{obs}}) = \log B , \tag{5}
\]

where we use \(\log B = \log (1 + z_{\text{obs}})\) for brevity.

Leavitt Laws relate oscillation periods of certain pulsating star types to absolute magnitudes \(M\). The most common functional form is linear in \(\log P\) and is used, for example, for classical Cepheid variables:

\[
M = a + b \cdot \log P , \tag{6}
\]
where \(a\) and \(b\) are calibrated using objects at known distances (ideally from geometry), for example, via \(Gaia\) parallaxes (Brown et al. 2018; Lindgren et al. 2018), detached eclipsing binaries in the LMC (Pietrzyński et al. 2019), or the parallax of the mega-maser in NGC 4258 (Humphreys et al. 2013).

Non-linear LLs have also been considered, for example, broken PLRs for Cepheids (e.g. Bhardwaj et al. 2016), PLRs affected by metallicity (e.g. Sesar et al. 2017; Gieren et al. 2018; Delgado et al. 2019, especially for RR Lyrae stars observed in the infrared). LLs are noticeably non-linear for Mira stars, where quadratic LLs have been used (e.g. Yuan et al. 2017; Huang et al. 2018):

\[
M = a + b_1 \cdot (\log P_{\text{obs}} - 2.3) + b_2 \cdot (\log P_{\text{obs}} - 2.3)^2. \tag{7}
\]

In the following, we adopt \(b = -3.26\) for a linear LL appropriate for Cepheids (
\(H\)-band Wesenheit PL-slope from R+16) and \(b_1 = -3.59\), \(b_2 = -3.40\), and \(\log P_{\text{ref}} = 2.3\) (Huang et al. 2018) for quadratic LLs.

Absolute magnitudes inferred using LLs, \(M_{LL}\), are biased by the effect of time dilation on oscillation periods, cf. Fig. 1. With Eq. 5 and Eqs. 6 & 7, we obtain

\[
\Delta M = M_{LL} - M_0 = b \Delta \log P = b \log B \tag{lin LL}
\]

\[
= b_1 \log B + b_2 \log B \left(2 \log P_{\text{obs}}' - \log B\right) \tag{quad LL}, \tag{8}
\]

where the second line applies to linear LLs and the third line to quadratic LLs. For linear LLs, the bias depends only on \(b\) and the observed heliocentric redshift. For quadratic LLs, RLB depends on \(z_{\text{obs}}\), \(b_1\), and \(b_2\), as well as the pivot period \(P_{\text{ref}}\), since \(\log P_{\text{obs}}' = \log P_{\text{obs}} - \log P_{\text{ref}}\).

The resulting bias in distance modulus is therefore:

\[
\Delta \mu = \mu_{LL} - \mu_0 = m - M_0 - \Delta M - m + M_0 = -\Delta M. \tag{9}
\]

Inserting Eq. 8 in Eq. 9 we obtain:

\[
\begin{align*}
\Delta \mu &= -b \log B \tag{[lin LL]} \\
\Delta \mu &= -b_1 \log B - b_2 \log B \left(2 \log P_{\text{obs}}' - \log B\right) \tag{[quad LL]}. \tag{10}
\end{align*}
\]

Figure 3 illustrates \(\Delta \mu\) for a wide range of \(z_{\text{obs}}\). We notice that a) \((\log B)^2 \sim 10^{-4}\) is negligible at distances < 100 Mpc, and b) \(\log P_{\text{obs}}'\) can be minimized by using a pivot \(P_{\text{ref}}\) close to the sample average. However, any galaxy is expected to show a distribution of Mira periods, so that time dilation could lead to a small apparent LL slope change in a given galaxy if redshift is not accounted for.

With \(\mu = 5 \log d + 25\) (in Mpc), the ratio of the true distance \(d_0\) to the biased distance \(d_{LL}\) is:

\[
d_0 = \frac{d_{LL,\text{lin}} \cdot 10^{0.2 \cdot b \log B}}{d_{LL,\text{quad}} \cdot 10^{0.2 \left[b_1 \log B + b_2 \log B \left(2 \log P_{\text{obs}}' - \log B\right)\right]}} \tag{12}
\]

for linear and quadratic LLs, respectively. Since \(b, b_1\), and \(b_2\) are all negative, and \(\log B \geq 1\), this typically means that \(d_0 < d_{LL}\). We notice that the term \(\log P_{\text{obs}}'\) can be negative or positive, depending on pivot period and average log \(P_{\text{obs}}\). In the following, we consider the small difference between \(\log P_{\text{ref}} = 2.3\) and \(\log (P_{\text{obs}}) = 2.4\), which corresponds to the case of Miras in NGC 4258 (Huang et al. 2018, ‘Gold’ sample in their Tab. 6).

Figure 4 illustrates RLB as a function of distance assuming \(H_0 = 74 \text{ km s}^{-1} \text{ Mpc}^{-1}\) and redshift caused by cosmic expansion only. The slightly steeper slopes of Mira LLs imply a slightly stronger susceptibility to RLB compared to Cepheids. For quadratic LLs, more significant differences result from possible differences among the average observed and pivot period (if \(\log P_{\text{obs}}' \neq 0\)).

\(H_0\) is measured as the intercept of the Hubble diagram, \(a_\alpha\) (cf. Eqs. 5 and 9 in R+16, subscript \(x\) denotes photometric band) via

\[
\log H_0 = \frac{M_0^x + 5a_\alpha + 25}{5}, \tag{13}
\]

With Eq. 13 and \(\Delta M = M_{\text{true}}^x - M_{x,\text{obs}}^0\), we obtain:

\[
H_{0,\text{true}} = H_{0,\text{LL,lin}} \cdot 10^{-0.2 b \log B} \tag{14}
\]

for linear and quadratic LLs, respectively, where \(H_{0,\text{true}} > H_{0,\text{LL}}\) since \(b, b_1, b_2\) all < 0, and \(\log B = \log (1 + z_{\text{obs}}) > 0\). Hence, the Universe is expanding slightly faster than previously reported based on the Cepheid-based distance ladder (R+16, Riess et al. 2018, 2019; Reid et al. 2019). In \(\S 3\), we estimate this effect and the correction for \(H_0\), and underline the importance of correcting variability periods for time dilation when measuring distances exceeding 40 Mpc using Mira stars with JWST.
3. Correcting $H_0$ for RLB

We now estimate RLB as it applies to the SH0ES Cepheids-based distance ladder (R+16) and the corresponding $H_0$ measurement. To this end, we compiled measured heliocentric redshifts from NED\(^1\) as well as other relevant information for the anchor and SN-host galaxies. Table 1 provides this information for convenience.

We first determine the difference between the mean redshift of LL anchor galaxies and the mean redshift of SN-host galaxies used for measuring $H_0$. The $\sigma_{PL}$-weighted average observed redshift of anchor galaxies is $\langle z_{obs,cal} \rangle = 0.48 \times 10^{-3}$. For Milky Way Cepheids, we adopt $v_r = 0$ km s\(^{-1}\), as expected for a random distribution of radial velocities. Any deviations from null velocity are on the order of 10 km s\(^{-1}\) and can be comfortably neglected. For SN-host galaxies, the $\sigma_{PL}$-weighted average redshift is $\langle z_{obs,LL} \rangle = 4.76 \times 10^{-3}$, and the average redshift difference between anchor and SN-host galaxies is $\Delta z_{obs} = 4.28 \times 10^{-3}$. In the following, we use $\log B = \log (1 + \Delta z_{obs})$ to calculate RLB and the bias of $H_0$.

Figure 5 shows $d_0/d_{LL}$ for all 19 SH0ES SN-host galaxies individually, as well as sample averages including the $\sigma_{PL}$-weighted average (dark red solid lines), the average weighted by number of Cepheids, $N_{cep}$ (dashed), and the un-weighted average (dotted). For the $\sigma_{PL}$-weighted average, we find $\langle d_0/d_{LL} \rangle = 0.979$. Using the $N_{cep}$-weighted average, we find $\langle d_0/d_{LL} \rangle_{N_{cep}} = 0.9974$. Any uncertainty contribution due to redshift uncertainties is minimal, since $\langle \sigma_z/\langle z \rangle \rangle = 0.004$ restricts variations in $\Delta \log P$ to $\lesssim 10^{-5}$.

For $H_0 = 73.50 \pm 1.40$ km s\(^{-1}\) Mpc\(^{-1}\) (Reid et al. 2019) and $\Delta z_{obs} = 4.28 \times 10^{-3}$, Eq. 14 yields $H_{0,true} = 73.70 \pm 1.40$ km s\(^{-1}\) Mpc\(^{-1}\), i.e., an increase of $\Delta H_0 = 0.20 \pm 0.01$ km s\(^{-1}\) Mpc\(^{-1}\). Thus, RLB amounts to 14% of the reported total uncertainty on $H_0$ of 1.90%. The small shift in $H_0$ slightly increases the significance of the tension between Planck and the SH0ES distance ladder from $4.1\sigma$ to $4.2\sigma$.

Analogously, we estimate biases of 0.19% and 0.20% for recent Mira-based $H_0$ measurements by Huang et al. (2019) that used linear Mira LL slopes of $b = -3.64$ and $-3.35$. In this case, NGC4258 was the sole anchor, and NGC1559 (Koribalski et al. 2004; $z_{obs,N1559} = 4.35 \times 10^{-3}$) the sole SN-host galaxy.

Of course, the above is a somewhat crude, first-order estimation of the degree by which previous $H_0$ measurements are affected by RLB. Future $H_0$ measurements should take into account the dilution of observed oscillation periods using Eq. 5 to avoid RLB. §4 highlights why this correction is required to elucidate Hubble tension using a future distance ladder based on more distant Mira stars.

4. Discussion

Time dilation can affect any oscillating star’s variability period and lead to distance bias whenever there is a net red-
shift difference among the LL calibration set and the population where LLs are being applied. Besides the aforementioned Cepheid, RR Lyrae, and Mira stars, many other classes of pulsating stars, including Scuti stars, type-II Cepheids, and long-period oscillating red giants obey PLRs that render them potentially useful as standard candles (e.g. Ziaali et al. 2019; Matsumaga et al. 2011; Kiss & Bedding 2003).

Mira stars are of particular importance due to their high luminosity and large amplitudes for future distance ladder calibration using JWST. Mira stars observed with JWST should significantly extend the distance d within which SNe Ia luminosity is cross-calibrated. Since volume increases as $d^3$, and the probability of a SN Ia exploding depends on volume, it follows that most new SN-host galaxies observed with JWST should reside at significantly greater distances and the probability of a SNIa exploding decreases accordingly, reducing the effect compared to Cepheids or Miras. According to Eq. 12, a mismatch between the average period of a sample of Miras and the pivot period of quadratic LLs can further increase RLB. Assuming log $P_{\text{LL}} = 2.3$, a bias of 1% is reached at 37, 42, 48, 57, 71, and 93 Mpc for locally calibrated Miras of log $P = 2.6$, 2.5, 2.4, 2.3, 2.2, and 2.1, respectively. Alternatively expressed, at 60 Mpc, individual Mira stars would be biased by between 0.7% and 1.7%, depending on their period.

RLB depends on LL slopes, which depend on photometric passbands. For example, the $H$-band LL in R+16 has slightly shallower slope ($b_H = -3.06$) than the near-IR Wesenheit LL ($b_{\text{W}} = -3.26$). Hence, the $H$-band Cepheid LL is less affected by RLB than the near-IR Wesenheit LL. Analogously, different kinds of oscillating stars exhibiting shallower LL slopes are also less strongly affected by RLB. For example, the slope of the period term in the RR Lyrae PL-metallicity relation has slope of approximately $-2.4$ (e.g. Barth et al. 2002; Minniti et al. 2003), reducing the effect compared to Cepheids or Miras.

Thankfully, RLB is easily avoided by correcting observed oscillation periods for time dilation effects. In the continued pursuit of measuring $H_0$ with 1% accuracy, this effect can and must be accounted for.

### Table 1

Information used to estimate redshift-Leavitt bias for anchor and SN-host galaxies in SH0ES Cepheids-based distance ladder (R+16). The number of Cepheids in each galaxy, $N_{\text{Cep}}$, approximate distance modulus $\mu$, and PL-relation dispersion $\sigma_{\mu}$, are all taken from R+16. Heliocentric redshifts $z_{\text{obs}}$ are compiled from NED, with original references Refz as follows: a: de Vaucouleurs et al. (1991), b: Meyer et al. (2004); Wong et al. (2006), c: Koribalski et al. (2004), d: Bureau et al. (1996), e: Krumm & Salpeter (1980), f: Guthrie & Napier (1996), g: Verheijen & Sancisi (2001), h: Lauberts & Valentijn (1989), i: Kent et al. (2008), j: Grogin et al. (1998), k: Strauss et al. (1992), l: Schneider et al. (1992), m: Richter et al. (1987). The redshift for the anchor galaxies and SN-host galaxies, weighted by $\sigma_{\mu}$, are shown above each entry. $\Delta z_{\text{obs,RF}} = z_{\text{obs}} - z_{\text{obs,cal}}$ is the redshift difference between each SN-host galaxy and the anchor reference frame. The shift in logarithmic oscillation period, $\Delta \log P$ (cf. Eq. 5), the overestimate of distance modulus $\Delta \mu$ (cf. Eq. 10), and the distance bias $\Delta d$ (cf. Eq. 11) are computed using $\Delta z_{\text{obs,RF}}$.

| Galaxy | $N_{\text{Cep}}$ | $\mu$ | $\sigma_{\mu}$ | $z_{\text{obs}}$ | $z_{\text{obs,RF}}$ | $\Delta \log P$ | $\Delta \mu$ | $\Delta d = d_0 - d_{\text{LL}}$ |
|--------|----------------|-------|----------------|----------------|----------------|----------------|-------------|----------------|
| Milky Way | 50 | -0.08 | 0 | | | | | -0.001 |
| LMC | 785 | 18.477 | 0.12 | 0.92 | b | - | - | |
| NGC 4258 | 139 | 29.397 | 0.15 | 1.49 | a | - | - | |
| Anchor galaxies, ($z_{\text{obs,cal}}$) = 0.48 $\times 10^{-4}$ |
| Milky Way | 50 | -0.08 | 0 | | | | | -0.001 |
| LMC | 785 | 18.477 | 0.12 | 0.92 | b | - | - | |
| NGC 4258 | 139 | 29.397 | 0.15 | 1.49 | a | - | - | |
| SN-host galaxies, ($z_{\text{obs,LL}}$) = 4.76 $\times 10^{-4}$ |
| NGC 1015 | 14 | 32.497 | 0.36 | 8.77 | b | 8.29 | 0.353 | 11.5 | -0.168 |
| NGC 1309 | 44 | 32.523 | 0.36 | 7.12 | c | 6.64 | 0.281 | 9.2 | -0.135 |
| NGC 3447 | 80 | 32.072 | 0.33 | 4.27 | e | 3.78 | 0.157 | 5.1 | -0.061 |
| NGC 2442 | 141 | 31.511 | 0.38 | 4.89 | b | 4.41 | 0.184 | 6.0 | -0.057 |
| NGC 3972 | 42 | 31.587 | 0.38 | 2.84 | g | 2.36 | 0.095 | 3.1 | -0.030 |
| NGC 3982 | 16 | 31.737 | 0.32 | 3.70 | a | 3.21 | 0.133 | 4.3 | -0.044 |
| NGC 4038 | 13 | 31.290 | 0.33 | 5.48 | h | 4.99 | 0.210 | 6.8 | -0.057 |
| NGC 3972 | 42 | 31.587 | 0.38 | 2.84 | g | 2.36 | 0.095 | 3.1 | -0.030 |
| NGC 3982 | 16 | 31.737 | 0.32 | 3.70 | a | 3.21 | 0.133 | 4.3 | -0.044 |
| NGC 4038 | 13 | 31.290 | 0.33 | 5.48 | h | 4.99 | 0.210 | 6.8 | -0.057 |
| NGC 3972 | 42 | 31.587 | 0.38 | 2.84 | g | 2.36 | 0.095 | 3.1 | -0.030 |
| NGC 3982 | 16 | 31.737 | 0.32 | 3.70 | a | 3.21 | 0.133 | 4.3 | -0.044 |
| NGC 4038 | 13 | 31.290 | 0.33 | 5.48 | h | 4.99 | 0.210 | 6.8 | -0.057 |
5. Conclusions

The Universe’s expansion leads to a subtle, distance-dependent dilation of variability periods in oscillating stars. If left uncorrected, this systematic change in variability period biases distance estimates based on Leavitt laws. When this effect is not accounted for, a future Mira-based distance ladder requires correcting variability periods for time dilation due to redshift becomes increasingly important. For the highly promising Mira stars, we estimate \( H_0 \) bias of order 2 – 3% if this effect is not accounted for. Hence, a future Mira-based distance ladder requires correcting variability periods for time dilation.

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