Adhesive force measurement of steady-state water nano-meniscus: Effective surface tension at nanoscale

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When the surface of water is curved at nanoscale as a bubble, droplet and meniscus, its surface tension is expected to be smaller than that of planar interface, which still awaits experimental studies. Here, we report static and dynamic force spectroscopy that measures the capillary force of a single nanoscale water meniscus at constant curvature condition. Based on the Young-Laplace equation, the results are used to obtain the effective surface tension (ST) of the meniscus, which decreases to less than 20% of the bulk value at the radius-of-curvature (ROC) below 25 nm, while indicating the bulk behaviour above ~130 nm ROC. Interestingly, such a possibility provides a qualitative resolution of the unsettled discrepancies between experiments and theories in the thermodynamic activation processes for the mentioned three types of nano-curved water. Our results may not only lead to development of microscopic theories of ST as well as further experimental investigations, but also help better understanding of the ST-induced nanoscale dynamics such as cluster growth or protein folding, and the ST-controlled design of nano-biomaterials using the nano-meniscus.

Surface tension (ST) is one of ubiquitous physical quantities that play a critical and central role in wide areas of science and engineering, ranging from nucleation of nano-bubbles to stabilization of proteins to controlled surface accumulation of compounds. Therefore, the microscopic understanding of ST is of much interest and importance because it consists of the long-standing and controversial questions concerning the physical characteristics of ST at nanoscale in contrast to bulk1–3. The first thermodynamic treatment of the spherical gas-liquid interface was given by Gibbs, which was extended by Tolman who obtained a widely-used, qualitative formula for the slight decrease of ST at the molecular-size scale4–6.

Despite extensive theoretical studies on the curvature-dependent ST reported thereafter3–8, however, it has been difficult to quantify such a dependence beyond the classical Tolman results, and there are still on-going debates on the validity of bulk ST (Fig. 1a) for nanoscale water. Moreover, there have been noticeable discrepancies between experimental results and theoretical predictions for the liquid-vapour phase-transition processes observed in the typical nanoscale systems of water (Fig. 1b,c,d), which remains unresolved and yet to be established experimentally3–8. Therefore, a well controlled experiment that quantifies the ST at nanoscale is in high demand, where the full-range and accurate capillary force measurement can be made. For this purpose, the water nano-meniscus is desirable due to its uniquely proven stability, controllability and force-sensitivity. Using the validity of the Young-Laplace equation at nanoscale10, our results of the measured total forces can be understood in terms of change of the ‘effective’ ST of water (refer to further discussions later).

Here, we employ the hybrid force-measurement system11 that combines a tapping-mode, amplitude-modulation atomic force microscope (AFM) and a microelectromechanical system (MEMS). It detects simultaneously the full-range dynamic as well as static forces associated with the capillary-condensed water nano-meniscus11. The values of the effective ST for the nanoscale menisci are derived by direct comparison of the measured interaction forces and the capillary force fitting based on the Young-Laplace equation12,13, whose validity at nanoscale has been justified by the accurate surface-force experiment14. We (i) observe gradual increase of the effective ST with ROC up to

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25-nm ROC, and (ii) show how the effective ST-based analysis provides a possible resolution of the afore-mentioned discrepancies (see discussion below)\textsuperscript{14,15}.

Figure 2a presents the experimental scheme of the system consisting of both the quartz-tuning-fork (QT-F)-based noncontact AFM (Fig. 2b) that measures accurately the force gradient and the MEMS sensor (Fig. 2c) that measures directly the full-range force\textsuperscript{11}. We first produce the nanometric water meniscus that is capillary-condensed as the AFM tip approaches the MEMS surface. The contact point ($z_c$) is determined as the position where the effective force gradients, elasticity ($k_{int}$) and damping coefficient ($b_{int}$), show drastic increase (Fig. 2d), where the tip is considered to make a hard contact with the MEMS.

Figure 3a shows the schematic geometry of the capillary meniscus formed in the tip-surface nano-gap. The total capillary force $F_t$ exerted by the meniscus is calculated by a sum of both the surface-tension force $F_s$ asso-

\[ F_s = 2\pi R_{tip} \gamma_m \left( -\sin \psi \sin(\theta_2 + \psi) - \frac{1}{2r_m} R_{tip} \sin^2 \psi \right) \]

(1)

where $R_{tip}$ is the tip’s ROC and $\gamma_m$ is the effective ST of meniscus. The contact angle $\theta_2$ will be assumed zero along with $\theta_2 \approx 0$ in the case of the hydrophilic silica surfaces (Supplementary S2). To investigate the interaction forces Eq. (1), one can consider constant either the pressure within the meniscus or the volume of the meniscus. The shape of the meniscus can be computed assuming constant volume, which is valid for fast retraction when there is not enough time to reach thermodynamic equilibrium. In this case, the ROC of the meniscus increases to keep the volume constant during tip retraction, while the local surface tension also changes accordingly, as the meniscus is elongated\textsuperscript{16}. On the other hand, for slow enough retraction, the ROC remains unchanged due to the stabilized (i.e. thermal equilibrium) pressure difference across the water/vapour interface at constant pressure, and also the surface tension is maintained constant during retraction, both of which can be obtained by best fit of the experimental curves. In our experiment, the retraction speed of the MEMS plate is less than 1 nm/s, more than $10^3$ times slower than that employed to keep the meniscus volume constant\textsuperscript{16}. Therefore, in our analysis, we treat the meniscus’ ROC, $r_m$, as a variable to determine the best fitting value of ST, $\gamma_m$, by direct comparison of force measurements and numerical simulations. Note that we assume the capillary force is much higher than the van der Waals force, gravity force (Supplementary S3), and electrostatic force. We ignored the electrostatic force induced by surface charge density in the thin surface hydration-layers since it is about 100 times smaller than the measured force\textsuperscript{15}. In particular, we extract the surface tension from Eq. (1) for a water column of at least 7 nm long, whose center is far enough to neglect the influence of electrostatic force. Therefore, we consider that the surface tension we obtain corresponds to the value of the gas-liquid interface at the meniscus equator, rather than the value near the surfaces where surface charge effects may contribute (see also Supplementary S3).
Figure 3b presents four typical (snapshot) configurations of water menisci being elongated during very slow (<1 nm/s) retraction of the MEMS plate for force measurement, where each ROC is numerically evaluated by the Young-Laplace equation.\(^1\) As shown, the initial value of \(r_m\) is maintained constant during retraction until its rupture, that is, the ROC is invariant from red to yellow to green to blue as the tip is retracted. Figure 3c demonstrates the validity of the constant ROC (or constant \(r_m\)) condition by quantitative comparison of the measured forces with the theoretical ones that assume either constant curvature (\(F_{\text{curvature}}\)) or constant volume (\(F_{\text{volume}}\)). As shown, the experimental force-distance curve matches excellently with the numerical simulation for constant curvature, but deviates severely from that under constant volume.\(^{16,17}\) Therefore, the isobaric assumption is appropriate for very slow retraction, which also justifies the constant \(r_m\) during the entire force measurement as the meniscus is stretched (Fig. 3b). Notice that in our previously reported time-resolved measurement of activation time for nucleation\(^1\) as well as rupture\(^1\) of a water nano-meniscus, each data point was taken at every 10 ms to 20 ms at a fixed position above the substrate, which was long enough to exhibit steady-state response at thermal equilibrium without any abrupt temporal variation of data except at nucleation or rupture. In other words, the speed of the tip (sampling time) was as slow (long) as that of the present work, which justifies our assumption of constant ROC or steady-state state of the nano-meniscus.

Figure 4a presents the typical force-measurement result of the MEMS sensor, from which one can determine uniquely \(\gamma_m\) for a given \(r_m\) such that the best fitting is obtained only for a specific pair of both values (see Supplementary S1). Note that \(r_m\) (meniscus’ radius of curvature) is constant during meniscus experiment and gives the information of \(z_0\) for the rupture distance, from which we can derive the volume of the meniscus according to the Young-Laplace equation for the capillary bridge\(^1\) having constant \(r_m\) (Supplementary S4). Interestingly, we find the fitted value of \(\gamma_m\) for \(r_m = 19\) nm in ambient condition is about 9.59 mN/m. Figure 4b plots various \(\gamma_m\) for several different \(r_m\) of the menisci, obtained by the same procedures described in Fig. 4a. We have varied relative humidity (~60%) while other conditions are fixed as 1 atm and room temperature (~23.5 °C), each data point in Fig. 4b is given by individual experiment. As observed, \(\gamma_m\) increases in approximately linear proportion with \(r_m\) up to 25 nm (red circle indicates the data of Fig. 4a) and a simple extrapolation shows the bulk
value at \(~130\) nm ROC (see inset). Figure 4a represents single approach/retraction experiment data for single water meniscus. And Fig. 4b plots each data point of single approach/retraction experiment varying with relative humidity, which determines the size (volume) of the meniscus. Even at single approach/retraction experiment, the meniscus volume can change with respect to variation of \(z_0\) in equilibrium meniscus in the constant condition (Supplementary S4).

Let us first justify calculation of the force under the assumption of constant curvature for the meniscus. Equation (1) is calculated by numerical solution of the Young-Laplace equation\(^1\), which provides the steady-state configuration of the axially symmetric liquid-vapour interface. For fast retraction, the meniscus is not in thermal equilibrium and thus its shape can be computed under constant volume\(^1\), for which the neck diameter decreases with elongation. However, sufficiently slow retraction leads to the stabilized (equilibrium) constant curvature during stretch (retraction), which is already confirmed by our previous work on the time-resolved experiment while sustaining the signal responses at every moment during retraction\(^1\). Therefore, almost uniform mean \(r_m\) for a nanometrically small tip is calculated in Fig. 3b under the constant curvature condition, as confirmed in Fig. 3c. In our experiment, the retraction speed is below 1 nm/s, more than 1,000 times slower than for the constant-volume experiments\(^1\).

Let us now discuss the treatment of \(r_m\) as a variable. Recent AFM experiments on the capillary water-bridge have shown that \(r_m\) (\(\approx z_0/2\)) is much longer than the predicted Kelvin radius at a given relative humidity\(^1\), pronounced especially for water\(^2\), while that obtained by the surface force apparatus agrees well with the Kelvin equation\(^3\). This suggests that what we measured is the total forces of the meniscus resulting from capillary condensation as well as other effects such as coalescence due to the pre-adsorbed water layers or the double-layer forces\(^4\), which provides the information of the 'effective' surface tension, rather than the genuine value of surface tension (therefore, in order to investigate any physical change of surface tension of water, one has to separate out
bonding and dispersion force. ST exhibits the curvature dependence at nanoscale, as confirmed qualitatively indicates that since, at the molecular level, ST results from the interface interaction, associated with hydrogen

orders-of-magnitude compared to experiment, which can be similarly settled by the 30% of bulk ST that produces
cesses in nano-confined liquid, which may further contribute to practical applications such as the ST-controlled

by molecular dynamics simulations. Notice that the expected bulk value at room temperature, 71.97 mN/m) for various values of

m (i.e., meniscus sizes) at nanoscale. Each data point represents independent experiments performed for different sizes of the nano-menisus (the red dotted circle corresponds to the result obtained by the data of Fig. 4a). Notice that the simple extrapolation of the data shown in the inset of 4b expects the bulk-value behaviour of the effective ST at above 130 nm.

the additional effects, which is beyond the scope of our current work and may be considered as a future work). To incorporate this observation in our analysis, we vary \( r_m \) to find the capillary force. Wide variation of \( r_m \), which is numerically calculated for a given rupture distance (or meniscus size), allows one to determine the unique pair of \( r_m \) and \( \gamma_m \) that best fit the experimental data. For example, \( \gamma_m/\gamma_{\text{bulk}} \approx 1/8 \) when \( r_m \approx 21.6 \text{ nm} \) (Fig. 4a). This indicates that since, at the molecular level, ST results from the interface interaction, associated with hydrogen bonding and dispersion force, ST exhibits the curvature dependence at nanoscale, as confirmed qualitatively by molecular dynamics simulations. Notice that the expected bulk value at \( r_m \approx 130 \text{ nm} \) (inset, Fig. 4b) is consistent with thermodynamics of the curved interface that predicts the bulk ST above ~100 nm.

Finally, we demonstrate that the curvature-dependent ST resolves the unsettled discrepancies of thermodynamic quantities in various nano-water systems. For example, the calculated tensile strength for vapour-bubble formation by the nucleation-rate theory is about 1,800 atm, much larger than the measured 277 atm. This disagreement can be resolved if the ST assumes 30% of the bulk value, in qualitative agreement with our results as well as with other expected value of 22% in the cluster-formation model of bubble (Supplementary S5). For nano-droplet formation in the supersaturated vapour, the theoretical nucleation rate is underestimated by two orders-of-magnitude compared to experiment, which can be similarly settled by the 30% of bulk ST that produces 4.6-times decrease of the vapour-nucleation energy-barrier, resulting in the 100-fold rate increase. For the water nano-menisus under the shear-mode AFM that is insensitive to the capillary force, the estimated energy barriers for both capillary condensation and rupture are about 4–5 times smaller than the theoretical values, which can be also resolved by the 20–25% of bulk ST (Fig. 4b), similarly to the nano-droplet formation.

We have quantified the effective ST behaviour at nanoscale by measurement of the total capillary force resulting from the water nano-menisus, in combination with theoretical calculation of the meniscus ROC based on the Young-Laplace equation. We have shown that the substantially reduced values of the effective ST at nanoscale may resolve the existing discrepancies between experiments and theories associated with the thermodynamic phase-transition effects in three types of nano-confined water. These observations may trigger theoretical development for a better understanding of surface tension at the molecular level. They will allow a novel guidance to the general ST-related phenomena including growth dynamics of liquid nano-clusters and biological processes in nano-confined liquid, which may further contribute to practical applications such as the ST-controlled self-assembly of bio-molecules and the efficient design of nano-biomaterials using the surfactant-like effect of ROC.

Methods

AFM-MEMS combined system for accurate force measurement. In our system, the QTF-AFM detects the dynamic force gradient that provides information on the viscoelasticity of the meniscus, while the MEMS sensor obtains simultaneously the absolute static force in the full distance range. The hydrophobic quartz tip, which has an ROC of ~50 nm, is fabricated by a commercial puller (P-2000, Sutter Instruments Co.) and attached to the bottom of QTF for small amplitude-modulation (AM) operation of AFM in the tapping mode. The QTF probe allows stable force measurement for several menisci of different sizes by varying relative humidity within the condition of constant \( r_m \) without making any direct contact of the tip with the surface, unlike the case of Fig. 3c where the tip contacts the surface before retraction to measure the contact point \( z_c \). (b) Ratio of the effective ST, \( \gamma_m/\gamma_{\text{bulk}} \) is the bulk value at room temperature, 71.97 mN/m) for various values of \( r_m \) (i.e., meniscus sizes) at nanoscale. Each data point represents independent experiments performed for different sizes of the nano-menisus (the red dotted circle corresponds to the result obtained by the data of Fig. 4a). Notice that the simple extrapolation of the data shown in the inset of 4b expects the bulk-value behaviour of the effective ST at above 130 nm.

Figure 4. Determination of the best fits for the effective ST, \( \gamma_m \), at nanoscale. (a), The typical experimental force curve is compared with the numerical solution of Eq. (1) based on the Young-Laplace equation under constant ROC for \( R_{\text{tip}} = 50 \text{ nm} \) and \( \theta_1 = 0 \) (supplementary S2), which allows unambiguous determination of the effective ST value \( \gamma_m \) as well as the ROC \( r_m \) of the water meniscus. Notice that we have repeated similar force measurement for several menisci of different sizes by varying relative humidity within the condition of constant \( r_m \) without making any direct contact of the tip with the surface, unlike the case of Fig. 3c where the tip contacts the surface before retraction to measure the contact point \( z_c \). (b) Ratio of the effective ST, \( \gamma_m/\gamma_{\text{bulk}} \) is the bulk value at room temperature, 71.97 mN/m) for various values of \( r_m \) (i.e., meniscus sizes) at nanoscale. Each data point represents independent experiments performed for different sizes of the nano-menisus (the red dotted circle corresponds to the result obtained by the data of Fig. 4a). Notice that the simple extrapolation of the data shown in the inset of 4b expects the bulk-value behaviour of the effective ST at above 130 nm.
amplitude, \( k \) the stiffness of the tip, \( \omega \) the drive frequency, \( \omega_0 \) the resonance frequency, \( z_r \) the tip-sample separation, \( A \) the tip’s oscillation amplitude and \( \theta \) phase shift of the oscillation. The force measured by AFM is thus

\[
F_{\text{AFM}} = \int_0^{z_0} \sin(\omega t - k z) \, d\phi + F_0,
\]

where \( z_0 \) is the rupture distance and \( F_0 \) is a constant, whereas the total capillary force that the MEMS detects is simply

\[
F_{\text{MEMS}} = -k_{\text{MEMS}} \Delta x,
\]

where \( \Delta x \) is the meniscus-induced displacement of the MEMS’ upper plate (made of silica) and the stiffness is \( k_{\text{MEMS}} = 2.43 \pm 0.01 \text{ N/m} \) that is about 10 times stiffer than the water meniscus\(^{11}\). Notice that the two values, \( F_{\text{MEMS}} \) and \( F_{\text{AFM}} \), have been shown to provide exactly the same results\(^{11}\) (details described in the reference) by a proper assignment of the integration constant \( F_0 \).

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Author Contributions

S.K. and S.A. carried out experiments. W.J. designed and directed the research. S.K., B.K., W.L., H.K. and W.J. analysed and interpreted the data. S.K. and W.J. wrote the manuscript.

Additional Information

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