Effect of Cleaning the Annular Space on the Adhesion of the Cement Sheath to the Rock

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Abstract: Drilling boreholes in gas zones and in zones with the possibility of migration or gas exhalation requires a high index of well tightness. An important parameter determining the effectiveness of sealing the annular space is the adhesion of the cement sheath to the rock formation. Low values of adhesion of the cement sheath to the rock formation and to the casing surface result in the formation of uncontrolled gas flows. The lack of adhesion also reduces the stabilization of the pipe column. To obtain the required adhesion, the annular space should be properly cleaned. Thorough removal of filter cake from the drilling fluid increases adhesion and reduces gas migration from the annular space. Therefore, in this work, the authors focus on determining the effect of cleaning the annular space on the adhesion of the cement sheath to the rock formation. The results of the research work allow for further research on the modification of spacers and cement slurries in order to obtain the required increase in adhesion. The article presents the issues related to the preparation of the borehole for cementing by appropriate cleaning of the rock formation from the residue of the mud cake. During the implementation of the works, tests of cleaning the rock surface are performed. The obtained results are correlated with the results of adhesion on the rock–cement sheath cleaned of the wash mud cake contact. When analyzing the obtained test results, a relationship is found between the cleaning of the rock surface and the adhesion of the cement sheath to it.

Keywords: improving the sealing of the borehole; rational selection of drilling fluids; well cementing; cleaning the borehole; adhesion; cement sheath; spacer fluid

1. Introduction

1.1. Purpose of the Work and Literature Background

Cementing of the casing column is performed in order to seal the annular space, i.e., to isolate the gas, oil and aquifers levels. The lack of such tightness makes it possible to create out-of-pipe flows of reservoir media or prevent the exploitation of natural gas [1–4]. In order to properly insulate the annular space, the cement slurry is pressed in. After it is bonded to the rock formation and to the surface of the casing, it guarantees the required tightness. However, this tightness also depends on the adhesion of the cement sheath to the contact surface. According to the literature [5,6], good grip means that there is no gap or no free movement of two bodies in relation to each other. It is interpreted in the contact plane with simultaneous action of tearing, compressive or shear stresses from the outside [5,7,8].

1.2. Factors Influencing the Adhesion of the Cement Sheath

When analyzing the conditions in the borehole, the resulting types and directions of force action in relation to the contact surface of the cement sheath and pipes are distinguished [9]. In the borehole, there are forces with the direction of action perpendicular to the contact surface and the forces acting in the direction parallel to these surfaces, analyzed later in this publication. These forces are caused by the elongation or contraction of the...
pipes due to temperature changes. They can also be the result of the formation of resistances preventing the mutual displacement of pipes [9–11]. The parameter of adhesion is the slip resistance determined in the tests by the vertical movement of the steel pipe or the rock core in the hardened cement slurry, as shown in Figure 1.

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The factors that affect the adhesion of the hardened cement slurry to the contact surface are mainly [9,12–14]:

- Tight adhesion of the cement sheath to the contact surface;
- Positive volume increase of the setting cement slurry;
- Gelling of the cement slurry on contact with the hydrated subsurface layer of the rock formation;
- The pressure exerted by the casing pipes on the setting cement slurry by cooling the pipes with the pumped liquids and then expanding them due to the temperature increase during the setting of the cement slurry;
- Adhesion forces between cement slurry and pipes;
- Bonding of the cement slurry to the surface of the pipes and the surface of the rock formation due to the penetration of slurry into the cavities resulting from the roughness of the contact surface.

In turn, the reduction of the adhesion value of the cement sheath to the contact surface is influenced by:

- Shrinkage of cement slurry during setting;
- Fluctuations in pressure and temperature during the setting of the cement slurry resulting, inter alia, from closing the cement head after the completion of cementing and leaving the pipe column at the final pressure of the treatment;
- Injection into the borehole of a cold scrubber when drilling cement plug;
- Low surface roughness coefficient of pipes [15–18].
However, from the point of view of preparing the borehole for cementing, the non-
displaced mud layer has a significant influence on the adhesion of the cement sheath. It
blocks the wetting of the surfaces in contact with the cement slurry due to the formation
of adhesion forces at the interface [19]. Moreover, the unremoved mud cake after mixing
with the cement slurry in the annular space reduces the mechanical strength of the cement
sheath [20–23]. It should be borne in mind that obtaining adequate tightness at the contact
of the cement sheath with the rock formation is influenced not only by the close adhesion
of individual layers (cement slurry to the wall of the borehole). Adhesion at the contact of
these layers also shows a strong influence [24,25]. Only the combination of both coface and
adhesion (adhesive and mechanical) allows the total to obtain the required contact tightness
effect of the cement sheath and the rock formation. Obtaining proper coface is not a problem
because the cement slurry with appropriately designed rheological parameters penetrates
the rock mass discontinuities resulting from drilling [8,26–28]. However, obtaining the
appropriate values of the second parameter, which is adhesion, requires appropriate
preparation of the annular space.

1.3. Preparation of the Borehole for Cementing

In the first stage, preparation of the borehole for cementing consists in lowering the
rheological parameters of the washer during rinsing [29,30]. Then, the spacer (washing
liquid) is pumped into the annular space in order to displace the drilling fluid and the
mud residue [31–33]. A very advantageous condition is that the casing column and the
drilled rock formation are moistened with the spacer. Such action improves the setting of
the cement slurry pumped over these liquids [34–36]. In order to thoroughly remove the
drilling fluid residues, washings consisting of a mixture of dispersants and surfactants are
used. The parameters of these spacers must be very precisely designed [37–41]. A number
of factors influence the efficiency of washing mud cake. These are, among others, contact
time of the spacer, spacer pumping rate, chemical composition of the spacer, concentration
of the agents used to prepare the spacer. The type of surface from which the mud cake is
removed, the type of drilling mud used for drilling and its technological parameters as
well as borehole conditions (temperature and pressure) are also important [37,42–46]. It
has been observed that obtaining an adequate cleaning of the annular space sometimes
contributes to the improvement of the tightness of the borehole.

The aim of the study is to determine the effect of cleaning the annular space on the
adhesion of the cement sheath to the rock formation. In order to obtain the required result,
it is necessary to thoroughly study the conditions in the cement sheath–rock formation
system. The obtained results are helpful in indicating the leading factor (adhesion or
adhesion) which determines the tightness. This allows to determine the effect of cleaning
the annular space on adhesion and introduce modifications to improve adhesion and obtain
adequate tightness of the borehole.

2. Materials and Methods

2.1. Materials

Four spacers and water as a control liquid were used to determine the effect of cleaning
the annular space on the adhesion of the cement sheath to the rock. The first liquid is a 0.5%
solution of SL372-ethoxylated alcohol C12–C15 (anionic surfactant from alkyl ether sulfate
group). The second liquid is a solution of 0.5% RL22-ethoxylated alcohol C12–C14 (non-
ionic surface-active compound used as emulsifier). The third liquid is CD-fatty alcohol
alkyl polyglucoside C8–C10. The fourth liquid called RL80 is ethoxylated alcohol C12–C14
(surface active agent used for wetting and as a non-ionic component of emulsifiers).

CEM I 42.5R Portland cement was used to prepare the cement slurry. This cement
is composed of 2.65% SO3 and 0.064% Cl−. Materials were also used to regulate the
parameters of the cement slurry. PSP 046 plasticizer is a dispersant based on modified
lignosulfonates and naphthalene with a bulk density of 440–550 kg/m3 and a pH value
ranging from 6.6 to 8.5. In order to remove air from the cement slurry, a defoaming agent
was used—a mixture of esters of unsaturated fatty acids and refined hydrocarbons. The start also included an antifiltrating agent and setting accelerator. Latex, which is a water dispersion of styrene-butadiene copolymer, was used to reduce the porosity of the cement sheath. Additionally, a latex stabilizer was added to the cement slurry. The matrix of the cement sheath was sealed with a 10% addition of microcement, which comes from Halliburton Micro Matrix. This type of microcement has grains smaller than or equal to 10 µm, and its specific surface area is approximately 1380 m²/kg. The percentage of means to prepare the cement slurry is summarized in Table 1.

Table 1. Recipe and parameters of the cement slurry used in the test of adhesion on the hardened cement slurry–rock contact.

| Ingredients | % by Mass of Cement |
|-------------|---------------------|
| Water–cement ratio | 0.46 |
| Plasticizer | 0.2 |
| Latex | 8.0 |
| Stabilizer | 1.0 |
| Defoaming agent | 0.48 |
| Antifiltrating agent | 0.22 |
| Setting accelerator | 4.2 |
| Microcement | 10.0 |
| Cement CEM I 42.5R | 100.0 |

All components in % by mass of cement.

2.2. Methods

2.2.1. Preparation of the Spacer (Washing Liquid)

To prepare the spacer, the following were used:

- The control spacer is water;
- Liquid No. 1 to 0.5% solution SL372-ethoxylated alcohol C12-C15 (anionic surfactant from alkyl ether sulfate group);
- Liquid No. 2 is a 0.5% solution of RL22-ethoxylated alcohol C12-C14 (non-ionic surface-active compound used as emulsifier);
- Liquid No. 3 to 0.5% solution CD-fatty alcohol alkyl polyglucoside C8-C10;
- Liquid No. 4 is a 0.5% solution of RL80-ethoxylated alcohol C12-C14 (surface active agent used for wetting and as a non-ionic component of emulsifiers).

To prepare the spacer, a certain amount of water was measured with a measuring cylinder. The water was poured into the mixer. The speed was set to 500 rpm and the specified amount of rinse aid was added.

2.2.2. Preparation of the Cement Slurry

For the effect of cleaning the annular space on the adhesion of the cement sheath to the rock, the samples of the cores after washing were sealed with cement slurry. The cement slurry was prepared as follows. A certain amount of water was measured out with a measuring cylinder. The water was placed in the mixer. The speed was set to 1600 rpm. The cement slurry agents were added to the mixing water and mixed for 10 min. Later, loose materials (microcement, cement) were dosed into the mixing water with chemicals and mixed for another 20 min. Mixing at low speed reflects slurry at well conditions.

2.2.3. Experimental Procedures

The properties of the cement slurry were tested in accordance with the standard:

- PN–EN ISO 10426-2. Oil and gas industry. Cements and materials for cementing holes. Lot 2: Testing of drilling cements. These tests include the following measurements: slurry density, filtration and thickening time.
The adhesion test was carried out according to the standard.

\[ \text{PN–EN 196-1: 2006 Cement testing methods. Compressive strength determination} \]

The test plan was adapted to the needs of the tests, the results of which allow to determine the effect of cleaning the annular space on the adhesion of the cement sheath to the rock. The drilling fluid flow simulator constructed at the Oil and Gas Institute-National Research Institute (Patent P.423842) was used for the tests. The device (Figure 2) allows to simulate the mud flow in the annular space. In this way, a washing mud cake was formed on the surface of the rock cores. The mud cake removal tests were carried out on four selected spacers, which were pumped at a rate of 11.2 L/min. This gives a Reynolds number of 3100. Water was used as the base spacer to determine the deposit removal checkpoint. The washing time was 4 min. The samples on which the mud cake was formed were three sandstone cores with an outer diameter of 25 mm and a length of 60 mm. They were fixed in a tripod inside a PVC pipe (Figure 2-left part of the photo) in a drilling fluid flow simulator.

![Figure 2. Drilling fluid flow simulator-view of the spacer pumping device.](image)

In the first stage, the degree of surface cleaning of the cores was determined by measuring the mass of the mud cake remaining on the cores after washing. The cores reflect the annular space of the borehole. The mass of the core before mud cake formation \((m_R)\) was determined, then the core with the mud cake \((m_{Ros})\) was weighed, and after pumping the spacer, the weight of the rock core with the residue of the spacer was determined again after pumping the spacer \((m_{Rpo})\). On the basis of the obtained results, the percentage effectiveness of the mud cake removal from the core surface was calculated according to formula:

\[ \text{Percentage effectiveness} = \frac{m_{Ros} - m_{Rpo}}{m_{Ros}} \times 100\% \]
\[
\% = 100 \cdot \frac{m_{Ros} - m_{Rpo}}{m_{Ros} - m_R}
\]  

(1)

where:
- \%—percent of sediment washout;
- \(m_R\)—core mass before the test (without mud cake);
- \(m_{Ros}\)—core mass with mud cake;
- \(m_{Rpo}\)—mass of the core with the residue of the mud cake (after washing);

In the tests, a mud cake from the PSK borehole was used to create a mud, which contained contaminants from the interval drilled into a 7-inch pipe section. Four spacers and a standard liquid–water spacer were used to determine the degree of deposit removal. Table 2 shows the results of the mud cake removal tests.

Table 2. The results of the research on the efficiency of the mud cake removal from the core surface and the adhesion of the cement sheath to the rock formation.

| Spacer                          | Measurement No. | Water | Spacer 1 | Spacer 2 | Spacer 3 | Spacer 4 |
|---------------------------------|-----------------|-------|----------|----------|----------|----------|
| Core weight before test \(m_R\), g | 1                | 68.65 | 68.64    | 68.65    | 68.66    | 68.66    |
|                                 | 2                | 68.68 | 68.65    | 68.64    | 68.64    | 68.66    |
|                                 | 3                | 68.65 | 68.65    | 68.66    | 68.65    | 68.65    |
| Core weight after mud \(m_{Ros}\), g | 1                | 72.58 | 72.52    | 72.5     | 72.47    | 72.44    |
|                                 | 2                | 72.55 | 72.5     | 72.52    | 72.4     | 72.89    |
|                                 | 3                | 72.54 | 72.44    | 72.47    | 72.43    | 72.75    |
| Core weight after spacer \(m_{Rpo}\), g | 1                | 70.44 | 69.52    | 69.49    | 69.65    | 69.44    |
|                                 | 2                | 70.38 | 69.6     | 69.49    | 69.72    | 69.43    |
|                                 | 3                | 70.37 | 69.58    | 69.47    | 69.72    | 69.4     |
| Washing percentage, \%          | 1                | 54.45 | 77.32    | 78.18    | 74.02    | 79.37    |
|                                 | 2                | 56.07 | 75.32    | 78.09    | 71.28    | 81.8     |
|                                 | 3                | 55.78 | 75.46    | 78.74    | 71.69    | 81.71    |
| Washing percentage (removal of mud cake) average value, \% | \(\bar{x}\) | 55.44 | 76.04    | 78.34    | 72.33    | 80.96    |
| Percentage increase in washing efficiency compared to the base value (washing with water), \% | \(\bar{x}\) | 0.00 | 37.16    | 41.31    | 30.47    | 46.03    |
| The average value of the adhesion of the cement sheath to the rock, MPa | \(\bar{x}\) | 0.696 | 0.928    | 0.957    | 0.870    | 0.986    |
| Percentage of adhesion increase in relation to the base value (adhesion after washing with water), \% | \(\bar{x}\) | 0.00 | 33.33    | 37.50    | 25.00    | 41.67    |
| The difference between the percentage increase in washing efficiency and the percentage increase in adhesion, \% | \(\bar{x}\) | 0.00 | 3.83     | 3.81     | 5.47     | 4.36     |

In the second stage of the research, the values of adhesion at the contact between the cement sheath and the rock core were determined. The tests were carried out for previously washed core samples and for the control sample, i.e., the core washed with water as the spacer. In order to determine the adhesion of the cement sheath to the sandstone core, after the mud cake was formed on it, and then, after washing with selected liquids, it was placed in a mold (Figure 3) and poured with cement slurry (Figure 4).
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![Figure 3. Core sample ready to be filled with cement slurry.](image1)

![Figure 4. Sample prepared for adhesion tests.](image2)

After 48 h of hydration, adhesion tests were performed on the contact between the hardened cement slurry and the rock core (cleaned of the previously produced mud cake). The adhesion test consists of placing a core sample sealed with cement slurry between the plates of a testing machine (Figure 5) and determining the breaking strength of adhesion on the hardened cement slurry–rock contact under the influence of a load applied to the sample.

The adhesion (MPa) on the contact between the hardened cement slurry and the rock core was calculated according to the Formula (2):

$$\sigma_p = \frac{P}{s} \cdot 10^{-3} \text{ [MPa]}$$

(2)

where:

- $\sigma_p$—contact adhesion hardened cement slurry–rock core (MPa),
- $P$—pressure force causing the connection to be broken at the contact of the hardened cement slurry with the rock (kN)—original record from a testing machine,
- $s$—contact surface of the rock sample with the cement slurry ($m^2$).
The adhesion (MPa) on the contact between the hardened cement slurry and the rock core was calculated according to the formula (2):

$$\sigma_p = \frac{P}{s} \text{[MPa]}$$  \hspace{2cm} (2)

where:
- $\sigma_p$—contact adhesion hardened cement slurry–rock core (MPa),
- $P$—pressure force causing the connection to be broken at the contact of the hardened cement slurry with the rock (kN)—original record from a testing machine,
- $s$—contact surface of the rock sample with the cement slurry ($m^2$).

The contact force ($P$) was read from the testing machine. The contact surface of the rock with the hardened cement slurry was equal to the value of the outer surface area of the core and the height of the cement slurry in the mold. Figure 6 shows the dimensions necessary to determine the contact surface of the rock with the hardened cement slurry. In order to obtain reliable results, all tests were carried out using a cement slurry of the same composition. The results of the adhesion tests obtained on the contact between the hardened cement slurry and the rock core are presented in Table 2.

$$s = \pi \cdot d \cdot h \text{ [m}^2\text{]}$$  \hspace{2cm} (3)

where:
- $d$—core diameter (m) for the conducted research is equal to 25 mm = 0.025 m;
- $h$—the height of the cemented part of the core for the conducted research is 44 mm = 0.044 m.
3. Results

The study of the mud cake removal efficiency begins with the determination of the value of the mud cake removal from the core surface with water (control test). This sample achieved a 55.44% removal of mud cake from the core surface. Then, tests of mud cake removal by various spacers were carried out. The obtained values of mud cake removal range from 72.33% for washing the cores with the spacer No. 3 to the maximum value, which is 80.96% after using the washing spacer No. 4 (Table 1). On the basis of the obtained results, the percentage increase in the washing efficiency in relation to the control sample is estimated at 55.44% (washing with water). The range of percentage increase in the mud cake leaching efficiency in relation to the base value, presented in Table 2, ranges from 30.47% to 46.03%. The results of the percent mud cake removal and the increase compared to the baseline value are summarized in Table 2 and Figure 7.

Another test is to determine the adhesion on the contact between the hardened cement slurry and the rock core cleaned of the produced washing mud cake. As in the previous test, first the adhesion of the control sample was determined. This is the adhesion after washing the core set with water as the spacer. The average of the adhesion values is 0.696 MPa (Table 2). Then, adhesion tests were carried out for samples washed by selected spacers. The average values of adhesion range from 0.87 MPa for the sample after the application of spacer No. 3 to the maximum value of adhesion, which is 0.986 MPa after washing the samples with the spacer No. 4 (Table 2 and Figure 7). The percentage increase in adhesion compared to the control sample ranges from 25% (spacer No. 3) to 41.67% (spacer No. 4). The results are presented in Table 2 and in Figure 7.

Additionally, an important interpretation is the difference between the percentage increase in the washing efficiency and the percentage increase in adhesion presented in the last row of Table 2. Values ranging from 3.81% to 5.47% were obtained. For such an interpretation, the percentage increase of the analyzed parameters (washing efficiency and adhesion) in relation to the base value was selected. This made it possible to determine the convergence of the analyzed values.
When analyzing the test results, it is stated that the values of the mud cake removal efficiency, i.e., the efficiency of cleaning the annular space, is proportional to the adhesion of the cement sheath to the rock formation. Therefore, a correlation analysis was performed to determine the degree of convergence between the compared features on the basis of the Pearson’s correlation coefficient. Pearson’s correlation coefficient is calculated on the basis of Formula (4), then according to Formula (5), the covariance (cov) was calculated, which determines the linear relationship between the analyzed variables \( x \) and \( y \), and the maximum likelihood estimator \( S_{dx}, S_{dy} \) giving the smallest deviation values (Formulas (6), (7), and Table 3). In the final step, the linear determination index (8) was calculated, which informs about the percentage of linearly expressed variability of the dependent variable by the independent variable. The interpretation of the strength of the correlation relationships is as follows:

Pearson’s correlation coefficient:

- below 0.2—weak correlation (practically no relationship);
- 0.2–0.4—low correlation (clear relationship);
- 0.4–0.6—moderate correlation (significant relationship);
- 0.6–0.8—high correlation (significant dependence);
- 0.8–0.9—very high correlation (very high correlation);
- 0.9–1.0—total correlation (practically full relationship).

\[
rx,y = \frac{\text{cov}(x, y)}{S_{dx} \cdot S_{dy}} \tag{4}
\]

where:

\( x \)—percentage values of elution (removal of mud cake) mean values (%);
\( y \)—value of the average adhesion of the cement sheath to the rock (MPa);
\( S_{dx}, S_{dy} \)—maximum likelihood estimators;
\( n \)—number of attempts.

Figure 7. List of the percentage increase of the analyzed parameters (the effectiveness of the removal of mud cake and adhesion on the contact between the hardened cement slurry–the rock core) in relation to the base value.
\[
\text{cov}(x, y) = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{n} \tag{5}
\]
\[
Sd_x = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n}} \tag{6}
\]
\[
Sd_y = \sqrt{\frac{\sum (y_i - \bar{y})^2}{n}} \tag{7}
\]
\[
WD = r_{xy}^2 \cdot 100\% \tag{8}
\]

After substituting to formulas
\[
\text{cov}(x, y) = \frac{46623}{5} = 0.930517
\]
\[
Sd_x = \sqrt{\frac{409.207}{5}} = 9.05
\]
\[
Sd_y = \sqrt{\frac{0.053}{5}} = 0.10
\]
\[
r_{xy} = \frac{0.930517}{9.05 \cdot 0.10} = 0.997623
\]
\[
r = 0.99 \in (0.9; 1.0)
\]
\[
WD = (0.997623)^2 \cdot 100\% = 99.53\%
\]

Table 3. Calculation data from the correlation of the mud cake removal efficiency to the adhesion of the cement sheath in contact with the rock formation.

| n | \(x_i\) | \(y_i\) | \((x_i - \bar{x})\) | \((y_i - \bar{y})\) | \((x_i - \bar{x})(y_i - \bar{y})\) | \((x_i - \bar{x})^2\) | \((y_i - \bar{y})^2\) |
|---|---|---|---|---|---|---|---|
| 1 | 55.44 | 0.696 | -17.2 | -0.2 | 3.29 | 295.22 | 0.04 |
| 2 | 76.04 | 0.928 | 3.4 | 0.0 | 0.14 | 11.68 | 0.00 |
| 3 | 78.34 | 0.957 | 5.7 | 0.1 | 0.40 | 32.70 | 0.00 |
| 4 | 72.33 | 0.87 | -0.3 | 0.0 | 0.01 | 0.09 | 0.00 |
| 5 | 80.96 | 0.986 | 8.3 | 0.1 | 0.82 | 69.52 | 0.01 |
| \(\Sigma\) | 363.11 | \(\Sigma = 4.437\) | \(\Sigma = 4.653\) | \(\Sigma = 409.207\) | \(\Sigma = 0.053\) |

\(x_i\)—readings of the percentage of elution (removal of mud cake) average values (%). \(y_i\)—value of the average adhesion of the cement sheath to the rock (MPa). Average values, \(\bar{x} = 72.6, \bar{y} = 0.90\).

Based on the correlation analysis of the obtained results of the research, the percentage increase in the effectiveness of mud cake removal to the percentage increase in adhesion, a strong match of the analyzed features is found. The value of linear regression R2 is in the range of the total correlation (Figure 8). Correlation analysis confirms the strong correlation between the increase in adhesion and the effectiveness of the removal of mud cake from the surface of the rock formation. The confirmation of the dependence of the analyzed features obtained on the basis of the test results allows us to state how strong the adhesion growth will be depending on the increase in the efficiency of cleaning the annular space. Additionally, the reverse relationship, i.e., how the efficiency of cleaning the space will increase on the basis of the obtained results of adhesion of the hardened cement slurry to the rock formation.
4. Discussion

The performed tests confirmed the necessity to properly prepare the annular space for the cementing procedure by effectively removing the residues of the washing mud cake. It was found that one of the most important factors determining the tightness and durability of the cement sheath is the proper cleaning of the annular space from the mud cake. A number of other factors that determine the effectiveness of sealing should be taken into account. These include the parameters of the drilling mud used for drilling, the composition, the type and parameters of the cement slurry, and the geological and technical conditions. Only a comprehensive analysis of all factors contributes to the expected results of work on improving the effectiveness of cementing.

5. Conclusions

Based on the research on the effect of cleaning the annular space on the adhesion of the cement sheath to the formation, it is concluded that:

1. The use of water for washing the geological structure from the washing mud cake formed on its surface results in the removal of approx. 55% of the washing mud cake.
2. Spacers selected for testing remove the washing mud cake formed on the surface of the cores in the range from 72.3% to 81%.
3. The obtained values of cleaning the surface of the core represent an increase in removal from 30.5% to 46% compared to cleaning the surface of the cores with water, which is used as the standard spacer.
4. The adhesion of the hardened cement slurry formulated for the tests to the rock core washed with water is 0.7 MPa.
5. The use of spacer selected for the purpose of testing allows to obtain adhesion on the contact between the hardened cement slurry–rock formation in the range from 0.87 to 0.99 MPa.
6. The percentage increase in adhesion compared to the base value ranges from 25% to 42%.
7. The difference between the percentage increase in washing efficiency and the percentage increase in adhesion shall not exceed the value of 5.5%.
8. On the basis of the obtained test results and the correlation analysis carried out, a very strong relationship is found between the cleaning of the annular space from the slurry mud cake and the adhesion of the hardened slurry to the rock formation.

Figure 8. The relationship between the efficiency of mud cake removal and the adhesion of the cement sheath on contact with the rock formation.
It should be borne in mind that despite the strong correlation between the cleaning of the annular space from the drilling mud cake and the adhesion of the cement sheath to the rock formation, a number of additional parameters determining the effectiveness of sealing the borehole should be taken into account. Therefore, each time before the cementing procedure is performed, specialized laboratory tests are carried out for specific geological and technological conditions.

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**Nomenclature**

| Symbol | Explanation |
|--------|-------------|
| %      | percent of sediment washout; |
| $m_R$  | core mass before the test (without mud cake); |
| $m_{R,R}$ | core mass with mud cake; |
| $m_{R,po}$ | mass of the core with the residue of the mud cake (after washing); |
| $d$    | core diameter (m) for the conducted research is equal to 25 mm = 0.025 m; |
| $h$    | the height of the cemented part of the core for the conducted research is 44 mm = 0.044 m; |
| $x$    | percentage values of elution (removal of mud cake) mean values (%); |
| $y$    | value of the average adhesion of the cement sheath to the rock (MPa); |
| $S_{d_{x}}, S_{d_{y}}$ | maximum likelihood estimators; |
| $n$    | number of attempts; |
| $x_i$  | readings of the percentage of elution (removal of mud cake) average values (%); |
| $y_i$  | value of the average adhesion of the cement sheath to the rock (MPa); |
| MPa    | megapascal; |
| KN     | kilonewton. |

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