Atomic and electronic structure of an alloyed topological insulator, Bi$_{1.5}$Sb$_{0.5}$Te$_{1.7}$Se$_{1.3}$

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Bi$_{2-x}$Sb$_x$Te$_2-y$Se$_y$ has been argued to exhibit both topological surface states and insulating bulk states, but has not yet been studied with local probes on the atomic scale. Here we report on the atomic and electronic structures of Bi$_{1.5}$Sb$_{0.5}$Te$_{1.7}$Se$_{1.3}$ studied using scanning tunnelling microscopy (STM) and spectroscopy (STS). Although there is significant surface disorder due to alloying of constituent atoms, cleaved surfaces of the crystals present a well-ordered hexagonal lattice with 10 Å high quintuple layer steps. STS results reflect the band structure and indicate that the surface state and Fermi energy are both located inside the energy gap. In particular, quasi-particle interference patterns from electron scattering demonstrate that the surface states possess linear dispersion and chirality from spin texture, thus verifying its topological nature. This finding demonstrates that alloying is a promising route to achieve full suppression of bulk conduction in topological insulators whilst keeping the topological surface state intact.

Topological insulators have attracted a tremendous amount of attention because of their peculiar surface states with spin chirality$^{1,2}$. The surface states of topological insulators arise from the non-trivial topology of the bulk electronic structure, whose existence and chiral nature (with spin-momentum locking), are protected by the topology. However, most topological insulators, such as binary compounds based on Bi and Sb, have exhibited metallic conductivity dominated by bulk carriers that originates from doping or formation of an impurity band by unintentional defects$^{3-7}$. This hinders the observation of novel physics from the topological surface states, because many theoretical proposals with respect to topological insulators are based on the assumption that the surface states, Fermi energy, and Dirac point are all located inside an energy gap without any bulk carriers$^{8,9}$. The realization of topological surface states in a bulk-insulating sample is therefore a critical step towards both fundamental studies and possible applications of topological insulators, such as realization of topological quantum computing through the generation of Majorana fermions$^{1,2,7}$.

Recently, a large bulk resistivity was realized in the Bi-based ternary compound, Bi$_2$Te$_2$Se$^{10}$. Clear signatures of the chiral surface states were observed, including spin polarization found by spin-polarized angle-resolved photoemission spectroscopy (ARPES)$^{11}$, the non-trivial Berry phase in quantum oscillations$^{16}$, and unique scattering properties of electrons observed by scanning tunnelling microscopy (STM)$^{12,13}$. Further improvement on the bulk-insulating properties was achieved in the quaternary compound, Bi$_{2-x}$Sb$_x$Te$_3-y$Se$_y$ (BSTS), where the Fermi energy was reportedly tunable by adjusting the stoichiometry of the four elements$^{14-18}$. Even though the amount of alloying is substantial, crystallinity of BSTS has been confirmed for a wide range of compositions$^{14}$, and the electronic properties (of BSTS) that stem from topological surface states have been observed by various methods, such as ARPES and electronic transport measurements$^{14-18}$. However, in contrast to Bi$_2$Te$_2$Se, where the ordering of chalcogens within a quintuple layer is considered to be important for reducing defects, the crystallographic order of BSTS is expected to be highly suppressed by alloying of chalcogens (Se and Te) and pnictogens (Bi and Sb). In this respect it is crucial to clarify whether the reduced structural order degrades the topological properties of the surface states by gaining local information on the atomic scale, something that has not yet been attained in BSTS$^{14,19}$.

Here we report on the first observations of the BSTS surface with STM and scanning tunnelling spectroscopy (STS). STM is a powerful technique for investigating surface states because of its extremely high spatial resolution and surface sensitivity. Many essential characteristics of topological insulators have been studied in binary
Figure 1 | Atomic structure and resistivity of the BSTS samples. (a), Crystal structure of Bi$_{2-x}$Sb$_x$Te$_{3-y}$Se$_y$, and optical image of the single crystal. (b), Temperature dependence of the resistivity of Bi$_{1.5}$Sb$_{0.5}$Te$_{1.7}$Se$_{1.3}$ samples, normalized by their room temperature values. In total, 5 crystals (S1-100 μm, S1-90 μm, S1-80 μm, S2-80 μm, and S2-140 μm) were cut and measured, where they were labelled with the sample batch (S1 and S2) and their thickness in μm. The inset shows the Arrhenius plot for the normalized resistivity; the solid lines are the fits at high temperatures, yielding an activation energy of ~30 meV.

Figure 2 | STM topographs. (a) and (b), STM topographs on a flat area where the step edges and atomic lattices were visible. In the inset of (a), a cross section of the topograph along the blue line marked ‘A’ is plotted. For (a), the scan size was 250 nm × 250 nm with a bias voltage, $V_B = 0.5$ V, and a set point current, $I = 1$ nA. For (b), the scan size was 10 nm × 10 nm with $V_B = -0.4$ V and $I = 0.2$ nA.
corrugations were not defects due to several characteristics that they possessed: firstly, the hexagonal lattice continued without disruption over the corrugations (see supplementary information, Fig. S1); secondly, the peak-to-peak variation in the height, 1.0 Å, was much smaller than the lattice constant; and finally, none of the corrugations showed a scattering wave emanating from them, which is typical for defects in other materials (Fig. 3a, c–i)\(^\text{19,26}\). These corrugations may be the result of small structural or electronic distortions caused by alloying. Actual defects on the surface were extremely rare: only a couple or so of them were observed in a 50 nm × 50 nm area. When they were observed, such defects typically appeared as atomic size protrusions or triangular shaped features, such as with other Bi and Sb based compounds\(^\text{19,26,29}\) (see supplementary information, Fig. S2).

The electronic structure of the sample can be unveiled through differential conductance \(g(r,E)\), measured by STS, where \(r\) is the position vector and \(E\) is the energy from the Fermi level inferred from the sample bias voltage, \(V_b\), as \(E = eV_b\) (where \(e\) is the electron charge). This quantity is proportional to the electron local density of states (LDOS) and the spatial map of \(g(r,E)\) at a certain energy reflects the variation of the LDOS. We obtained the conductance spectra at 256 × 256 regularly spaced points covering the area shown in Fig. 3a; Fig. 3b shows the average of the spectra taken. The averaged conductance spectrum is similar to typical trends for Bi\(_2\)Se\(_3\) and Bi\(_2\)Te\(_3\)\(^{18,19,22,28}\), which implies that they share a similar band structure with the topological surface state. The positions of the valence band (VB), conduction band (CB) and surface state (SS) were determined by comparing the STS data with previously reported ARPES data\(^\text{14}\), and substantiated by analyzing the Fourier transform (FT) of the conductance maps shown later in this paper (Fig. 4g). We interpret this spectrum as showing an energy gap of 300 meV that embraces the SS, as denoted in Fig. 3b. The boundaries between the bands are estimated to be located at ~40 meV for the VB and SS band, and at 260 meV for the CB and SS band. In contrast to typical semiconductors, there was a non-zero conductance inside the energy gap, with a dip that fits to the SSs with a cone shaped band observed by ARPES\(^\text{14}\). The minimum point of the conductance spectrum corresponds to the Dirac point, which was estimated to be at ~3 ± 19 meV. The amount of variation, 38 meV, is comparable to that measured in doped Bi\(_2\)Te\(_3\) and Bi\(_2\)Se\(_3\)\(^{14}\), and indicates that the topological surface states are well-preserved against a substantial amount of alloying.

To see the spatial dependence of the LDOS at different energies, maps of the differential conductance were taken for a bias voltage range of ~300 mV to ~600 mV in 20 mV steps. To enhance the observed features we plotted conductance maps at a normalized conductance, \(g_n = (g - \langle g \rangle) / \sigma_g\) (where \(\langle g \rangle\) and \(\sigma_g\) are the average and standard deviation of \(g\) in each map, respectively), so that the average of \(g_n\) was 0, and the standard deviation was 1. According to scattering theory, electrons on the surface of materials can be scattered by defects and make an interference pattern as a standing wave. This is often called quasiparticle interference (QPI)\(^{31–33}\), where scattering vectors, \(q\), of QPI have been measured in various materials\(^{26,21,10,34,35}\) and are directly related to the band structure of the materials. While the bulk states do not usually develop well-distinguished QPI patterns, because of the surface sensitive nature of the STM and possible scattering vectors having broad and continuous values, QPI by surface state electrons often appears as well-distinguished standing waves. Since topological surface states exist on the BSTS surface, a standing wave pattern from QPI is expected, as shown in Fig. 3e–i. That the wavelength of the standing wave becomes shorter as the bias increases reflects the dispersion of the topological surface states. This dispersion starts at around ~40 mV and continues up to the maximum measured bias of 600 mV (which implies the existence of surface states up to that energy). However, it should be noted that conductance maps below ~40 mV showed a drastic change where the corrugations shows no periodicity and no sign of QPI, indicating the disappearance of the surface state and a transition to the bulk valence band.

Detailed information of the QPI, such as the magnitude and direction of the scattering vectors, can be extracted from the Fourier transforms (FTs) of the conductance maps (or FT maps in short, Fig. 3j–p\(^\text{32}\)). The intensity in the FT map corresponds to the amount of QPI at a certain scattering vector \(q\)\(^\text{26,21}\). The FT maps may be divided into two different types: one above, and the other below ~40 mV. At a bias larger than ~40 mV, a high intensity region around the centre is observed that increases in size as the energy increases (Fig. 3i–p and 4g). At a bias below ~40 mV, on the other hand, the FT amplitude becomes extremely large (compared to FT maps for a bias above 40 mV), without the appearance of any prominent scattering vectors (Fig. 3j, k); also, see the normalized FT maps in supplement Fig. S3). This observation agrees with the band structure of the bulk valence band under ~40 mV, with topological

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**Figure 3** | **Conductance spectroscopy and maps.** (a), Topograph of the area where the conductance spectra were taken (50 nm × 50 nm, \(V_b = 0.6\) V, \(I = 0.5\) nA). (b), Plot of the average conductance spectrum over 256 × 256 regularly spaced points in (a), (c–i) and (j–p), Conductance maps generated from the spectra and their FTs, respectively (\(V_b = −300, −140, 0, 140, 280, 440\) and 600 mV). For the FT maps, the centre corresponds to the \(\Gamma\) point of the surface Brillouin zone; the horizontal line indicates the \(\Gamma-M\) direction. All the FT maps were fully symmetrised according to the symmetry of the lattice, and then low-pass filtered to reduce the speckle noise. The modulation voltage and frequency for the lock-in amplifier was \(V_{\text{mod}} = 5\) mV, and \(f_{\text{mod}} = 1,317\) Hz, respectively.
Figure 4 | Band structure and FT of the STS. (a), (c), and (e) are schematics of constant energy contours in k space, and (b), (d), and (f) are corresponding FT maps in q space, at $V_g = 440, 280,$ and $140$ mV, respectively. Prominent scattering vectors, such as the ones from backscattering ($q_b$) and the warping effect ($q_{wM}$ and $q_{wK}$), are plotted as dotted lines and solid lines, respectively. (g), A line-cut of the FT maps along the $\Gamma-K$ and $\Gamma-M$ directions stacked along the bias voltage, $V_b$. The colour scale indicates the amplitude of the FT, the $x$-axis corresponds to the scattering vector $q = |q|$, and the $y$-axis corresponds to $V_b$. A schematic of the band structure is drawn on the right hand side, where the bulk band is coloured in grey and the surface band is coloured in blue and red for spins up and down, respectively.

Discussion

Topological surface states are usually characterized by two unique features: the linear dispersion of the band with a degenerate energy where all bands converge to one point; and a spin texture where an electron with momentum $k$ has a unique spin direction perpendicular to $k^{\perp}$. To confirm these features, we compared the expected constant energy contours of the surface states in BSTS (Fig. 4a, c, e) to our FT maps (Fig. 4b, d, f). The constant energy contours were drawn with the assumption that the Fermi velocity, $v_F = 4.0 \times 10^5$ m/s, and the Dirac point, $E_D = 0$ mV, based on previously measured transport and ARPES results$^{3,4,16,17}$. Even though the FT maps showed high intensity spots at non-zero $q$, we found that none of them corresponded to the back-scattering vector $q_b$. Because back-scattering in the topological surface state is strictly prohibited (due to spin texture)$^{27}$, the absence of back-scattering is a strong indicator of the topological nature of the surface state.

If the surface state band had a perfect cone shape, there would be no high intensity point in the FT maps except at the $\Gamma$ point$^{27}$. Indeed, the FT maps taken at the energy near the Dirac point (i.e., $-40$–$160$ mV), showed no pronounced peak except at the origin (Fig. 3l, m). For energies higher than $180$ mV, however, high intensity peaks were observed at certain values of $q$, such as $q_{wM}$ and $q_{wK}$. This phenomena has been observed in various chalcogenides$^{31,12,26,30,38,39}$, and is well-described by the distortion of the topological surface state band from a perfect cone to a warped shape (usually called the “warping effect”)$^{27}$. As the surface state approaches the conduction band, the shape of the constant energy contours changes from a circle to a rounded hexagon, and then to a star shape (Fig. 4a, c, e). Warping of the constant energy contours results in two important effects: the distortion in spin texture with the out-of-plane component, and a nesting effect from the parallel part of the constant energy contours. Oblique scattering (that is not strictly prohibited by spin texture), is enhanced by these effects and gives a strong QPI that appears as high amplitude points in the FT maps (Fig. 4b, d, f).

The energy dependence of the electron scattering can be emphasized by plotting cross sections of the FT maps along the $\Gamma-K$ and $\Gamma-M$ directions stacked in the vertical direction for all measured energies (Fig. 4g). The high amplitude region shows a linear dispersion that crosses the $y$-axis at $E = 0$ mV, indicating a linear dispersion of the surface state with a Dirac point at $0$ meV. All the band structure information (including the energy range and dispersion of bulk and surface bands), as summarised in the schematic given on the right side of Fig. 4g, matches well with previous transport and ARPES results$^{3,4,16,17}$.

In summary, we have studied the electronic structure of a single crystal of the topological insulator, BSTS, which exhibited improved bulk-insulating properties due to alloying. STM measurements revealed an atomically flat surface with a hexagonal lattice. From STS measurements (including the resultant conductance maps and FTs), we confirmed the presence of a bulk energy gap and showed that it encompassed the Fermi energy and the surface state. QPI measured by FT maps indicated a linear dispersion and suppression of the back-scattering of electrons in the surface state. Our results clearly demonstrate that the topological nature of the surface state is robust against the alloying of the constituent elements. Chemical alloying, therefore, is a promising route to achieve full suppression of bulk conduction in topological insulators whilst keeping the topological surface state intact. These results suggest that BSTS could be a highly promising material as it exhibits both the Fermi energy within the bulk gap and a suppression of bulk carriers: requirements for many theoretical proposals for topological insulators.

Methods

Single crystals of Bi$_{1.5}$Sb$_{0.5}$Te$_{1.7}$Se$_{1.3}$ were grown by the self-flux method, in which high-purity starting materials (Bi, Sb, Te, and Se) were mixed and annealed according to a previously reported recipe$^{14}$. Samples were checked by energy dispersive spectroscopy and X-ray diffraction to verify the stoichiometry and high crystallinity.
respectively. The mobility of a thick flake cleaved from the sample reached 4,000 cm²/Vs at 4.2 K in a separate Hall measurement, which is comparable to other results reported on binary compounds. For STM measurements, a Unisoku low-temperature STM was used. The sample was cleaved in an ultrahigh vacuum chamber (~10⁻¹¹ Torr) at room temperature and then transferred to the low-temperature STM sample stage, where the temperature was kept at 2.8 K. Spectroscopy of the differential conductance was performed by a conventional lock-in technique.

1. Qi, X.-L. & Zhang, S.-C. Topological insulators and superconductors. Reviews of Modern Physics 83, 1057–1110 (2011).
2. Hasan, M. Z. & Kane, C. L. Colloquium: Topological insulators. Reviews of Modern Physics 82, 3045–3067 (2010).
3. Analytis, J. G. et al. Two-dimensional surface state in the quantum limit of a topological insulator. Nature 6, 960–964 (2010).
4. Chen, Y. L. et al. Experimental realization of a three-dimensional topological insulator, Bi₂Te₃. Science (New York, N.Y.) 325, 178–181 (2009).
5. Hsieh, D. et al. Observation of Time-Reversal-Protected Single Dirac-Cone Topological-Insulator States in BiₓTeₓ and SbₓTeₓ. Physical Review Letters 103, 146401 (2009).
6. Hsieh, D. et al. A topological Dirac insulator in a quantum spin Hall phase. Nature 452, 970–975 (2008).
7. Hsieh, D. et al. Observation of unconventional quantum spin textures in topological insulators. Science (New York, N.Y.) 323, 919–922 (2009).
8. Qi, X.-L., Li, R., Zhang, J. & Zhang, S.-C. Inducing a magnetic monopole with topological surface states. Science (New York, N.Y.) 323, 1184–1187 (2009).
9. Fu, L. & Kane, C. L. Superconducting Proximity Effect and Majorana Fermions at the Surface of a Topological Insulator. Physical Review Letters 100, 096407 (2008).
10. Ren, Z., Taskin, A. A., Sasaki, S., Segawa, K. & Ando, Y. Large bulk resistivity and surface quantum oscillations in the topological insulator Bi₂Te₃Se. Physical Review B 82, 241306 (2010).
11. Miyamoto, K. et al. Topological Surface States with Persistent High Spin Polarization across the Dirac Point in BiₓTeₓSe and BiₓSbₓTeₓ. Physical Review Letters 109, 166802 (2012).
12. Jia, S. et al. Defects and high bulk resistivities in the Bi-rich tetradymite topological insulator Bi₂₋ₓSbₓTe₃₋ₓSe. Physical Review B 86, 165119 (2012).
13. Nurmmat, M. et al. Unoccupied topological surface state in Bi₂Te₂Se. arXiv 5 (2013) at <http://arxiv.org/abs/1305.2341>.
14. Arakane, T. et al. Tunable Dirac cone in the topological insulator BiₓSbₓTe₃₋ₓSe. Nature communications 3, 636 (2012).
15. Segawa, K. et al. Ambipolar transport in bulk crystals of a topological insulator by gating with ionic liquid. Physical Review B 86, 075306 (2012).
16. Ren, Z., Taskin, A. A., Sasaki, S., Segawa, K. & Ando, Y. Optimizing BiₓSbₓTe₃₋ₓSe solid solutions to approach the intrinsic topological insulator regime. Physical Review B 84, 163311 (2011).
17. Taskin, A. A., Ren, Z., Sasaki, S., Segawa, K. & Ando, Y. Observation of Dirac Holes and Electrons in a Topological Insulator. Physical Review Letters 107, 016801 (2011).
18. Zhang, J. et al. Band structure engineering in (Bi₁₋ₓSbₓ)₂Te₃ ternary topological insulators. Nature communications 2, 574 (2011).
19. Alpichshev, Z. et al. STM Imaging of Impurity Resonances on BiₓSeₙ. Physical Review Letters 108, 206402 (2012).
20. Roushan, P. et al. Topological surface states protected from backscattering by chiral spin texture. Nature 460, 1106–1110 (2009).
21. Gomes, K. K. et al. Quantum Imaging of Topologically Unpaired Spin-Polarized Dirac Fermions. (2009) at <http://arxiv.org/abs/0909.0921>.
22. Cheng, P. et al. Landau Quantization of Topological Surface States in BiₓSeₙ. Physical Review Letters 105, 076801 (2010).
23. Hanaguri, T., Ishigami, K., Kawamura, M., Takagi, H. & Sasagawa, T. Momentum-resolved Landau-level spectroscopy of Dirac surface state in BiₓSeₙ. Physical Review B 82, 081305(R) (2010).
24. Jiang, Y. et al. Landau Quantization and the Thickness Limit of Topological Insulator Thin Films of SbₓTe₃₋ₓ. Physical Review Letters 108, 016401 (2012).
25. Honolka, J. et al. In-Plane Magnetic Anisotropy of Fe Atoms on BiₓSeₙ(111). Physical Review Letters 108, 256811 (2012).
26. Beidenkopf, H. et al. Spatial fluctuations of helical Dirac fermions on the surface of topological insulators. Nature Physics 7, 939–943 (2011).
27. Hor, Y. S. et al. Development of ferromagnetism in the doped topological insulator Bi₂₋ₓMnₓTe₃. Physical Review B 81, 195203 (2010).
28. Lee, J., Park, J., Lee, J.-H., Kim, J. S. & Lee, H.-J. Gate-tuned differentiation of surface-conducting states in BiₓSbₓTe₃₋ₓSeₙ topological-insulator thin crystals. Physical Review B 86, 245321 (2012).
29. Jiang, Y. et al. Fermi-Level Tuning of Epitaxial SbₓTe₃ Thin Films on Graphene by Regulating Intrinsic Defects and Substrate Transfer Doping. Physical Review Letters 108, 066809 (2012).
30. Alpichshev, Z. et al. STM Imaging of Electronic Waves on the Surface of Bi₂Te₃: Topologically Protected Surface States and Hexagonal Warping Effects. Physical Review Letters 104, 016401 (2010).
31. Heller, E. J., Crommie, M. F., Loss, D. P. & Eigler, D. M. Scattering and absorption of surface electron waves in quantum corals. Nature 369, 464–466 (1994).
32. Petersen, L. et al. Direct imaging of the two-dimensional Fermi contour: Fourier-transform STM. Physical Review B 57, R6858–R6861 (1998).
33. Fiete, G. A. & Heller, E. J. Colloquium: Theory of quantum corrals and quantum mirages. Reviews of Modern Physics 75, 933–948 (2003).
34. McElroy, K. et al. Relating atomic-scale electronic phenomena to wave-like quasiparticle states in superconducting BiSr₂CaCu₂O₈₋ₓ. Nature 422, 592–6 (2003).
35. Rutter, G. M. et al. Scattering and interference in epitaxial graphene. Science (New York, N.Y.) 317, 219–222 (2007).
36. Wray, L. A. et al. A topological insulator surface under strong Coulomb, magnetic and disorder perturbations. Nature Physics 7, 32–37 (2010).
37. Guo, H.-M. & Franz, M. Theory of quasiparticle interference on the surface of a strong topological insulator. Physical Review B 81, 041102(R) (2010).
38. Zhang, T. et al. Experimental Demonstration of Topological Surface States Protected by Time-Reversal Symmetry. Physical Review Letters 103, 266803 (2009).
39. Okada, Y. et al. Direct Observation of Broken Time-Reversal Symmetry on the Surface of a Magnetically Doped Topological Insulator. Physical Review Letters 106, 206805 (2011).
40. Fu, L. Hexagonal Warping Effects in the Surface States of the Topological Insulator Bi₂Te₃. Physical Review Letters 103, 266801 (2009).
41. Qu, D.-X., Hor, Y. S., Xiong, J., Cava, R. J. & Ong, N. P. Quantum oscillations and hall anomaly of surface states in the topological insulator Bi₂Te₃. Science (New York, N.Y.) 329, 821–824 (2010).

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Author contributions
W.K., I.J., J.S.K. and H.S. conceived and designed the experiments. J.P. and J.S.K. prepared the samples. S.W.H., I.J., J.S.K. and H.S. provided advice on the project. All authors discussed the results and commented on the manuscript.

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