Ultra-Low-Frequency (ULF) waves provide a means for the rapid propagation of energy and field-aligned current in planetary magnetospheres. At Earth, the ULF frequency range is usually defined as including waves with periods of 0.2–600 s; however, at Jupiter these waves can extend to periods of tens of minutes. In both magnetospheres, shear mode Alfvén waves can form field line resonances that exist between the ionospheres, with periods of a few minutes at Earth and a few tens of minutes at Jupiter. A major distinction between these two magnetospheres is in the density distribution. Earth has a dense ionosphere full of heavy ions, an extended, cold plasmasphere and a relatively low-density plasma sheet. In contrast, at Jupiter, the ionosphere is largely hydrogen (both in atomic form and in the H$_3^+$ molecular ion), there is no appreciable plasmasphere and the plasma disk is dense and populated with heavy ions (largely sulfur and oxygen) originating at the moon Io and to some extent from other moons. As at Earth, the sharp Alfvén speed gradient above the ionosphere forms an ionospheric Alfvén resonator at Jupiter with periods of seconds. Furthermore, the high-latitude lobes at Jupiter have very low density and a resonant structure can be formed by waves bouncing between the ionosphere and the dense plasma disk. This structure leads to periods of tens of seconds. Finally, the dense Io plasma torus and plasma sheet provide conditions for compressional cavity modes to form in this region. Thus, the structure of the field line resonance modes is quite different at the two planets. Implications of these resonances on auroral particle acceleration will be discussed.

Keywords: ULF waves, magnetospheres, Earth, Jupiter, Alfvén waves, particle acceleration

INTRODUCTION

Ultra-low-frequency (ULF) waves are ubiquitous in the magnetospheres of Earth and Jupiter, and their presence in other magnetized planets is very likely. These waves, defined at Earth as having periods from 0.2 to 600 s (e.g., Kivelson, 1995), play a major role in transporting energy and momentum throughout the magnetosphere, as well as mediating changes in the field-aligned currents. ULF waves are generally described using the theory of magnetohydrodynamics (MHD), which allows for three distinct wave modes, labelled the slow (or ion acoustic) mode, the intermediate (or shear Alfvén) mode, and the fast (or magnetoacoustic) mode. On a global scale, the slow mode does not play a major role, and so the rest of this review will concentrate on the Alfvén and fast mode.

In MHD theory, the shear Alfvén mode is guided along the magnetic field, and carries a field-aligned current. This mode propagates along the field line at the Alfvén speed, defined as...
\[ \frac{\omega}{k_1} = V_A = \frac{B}{\sqrt{\mu_0 \rho}} \]  

(1)

where \( \omega \) is the wave frequency, \( k_1 \) is the wave number along the magnetic field, \( B \) is the magnetic field strength, and \( \rho \) is the mass density. On closed magnetic field lines, this wave can propagate from one ionosphere to the conjugate ionosphere forming a standing wave between the two ionospheres. When such a structure is excited by mode coupling from a fast mode wave, it is called a field line resonance (Chen and Hasegawa, 1974; Southwood, 1974). Since the magnetic field strength, the mass density, and the length of the field line vary from one field line to the next, this mode creates a range of frequencies that can be used as a proxy for the mass density along the field line. The study of these frequencies to determine the mass density has been termed “magnetoseismology” (e.g., Menk and Waters, 2013).

On the other hand, the fast mode propagates more isotropically, so that it is not guided along a field line, with a dispersion relation in a low-\( \beta \) plasma (with \( \beta = 2\mu_0 B^2 / \rho c^2 \) being the ratio of plasma pressure to magnetic field pressure) given by

\[ \omega^2 = k^2 V_A^2 + k^2 c_s^2 \]  

(2)

Here \( k \) is the total wave number, \( k_1 \) is the perpendicular wave number and \( c_s \) is the sound speed. Since this mode can propagate in all directions, it will tend to fill up any regions of space. Due to the inhomogeneity of magnetospheric plasmas, this mode can form resonant cavities in regions where the plasma density is significantly different from the surrounding regions.

Since ULF waves have wavelengths that can be comparable to the size of the whole magnetosphere, the standard Wentzel-Kramers-Broulliin (WKB) theory (e.g., Stix, 1992), which implies that the wave propagates without reflection when the gradient scale length of the wave speed is much longer than the wavelength, is violated. In the limit of a discontinuous change in the Alfvén speed (for the shear mode) or the magnetosonic speed (for the fast mode), the reflection coefficient can be written as

\[ R = \frac{E_{inc}}{E_{ref}} = \frac{V_2 - V_1}{V_2 + V_1} \]  

(3)

Here \( V_1 \) is the wave speed in the incident region and \( V_2 \) is the wave speed in the outer region. In a similar manner, for reflections of shear Alfvén waves from the ionosphere, the reflection coefficient can be written as

\[ R = \frac{1 - \mu_0 V_A \Sigma_p}{1 + \mu_0 V_A \Sigma_p} = \frac{\Sigma_A - \Sigma_p}{\Sigma_A + \Sigma_p} \]  

(4)

where \( \Sigma_p \) is the Pedersen conductance and \( \Sigma_A = 1/\mu_0 V_A \) is sometimes called the “Alfvén conductance.” It should be noted that in the presence of a finite Hall conductance in the ionosphere, the Pedersen conductance in Equation 4 can be modified by a term describing the coupling of the shear Alfvén wave to the fast mode (e.g., Lysak and Yoshikawa, 2006).

Equations 3 and 4 indicate that the strongest reflections occur when the discontinuity in the wave speed is very large, or in the case of the ionosphere, if the Alfvén conductance is very different than to the Pedersen conductance. As a reference point, it can be noted that an Alfvén speed of 1,000 km/s corresponds to 0.796 mho, or a conductance of 1 mho corresponds to 796 km/s. Therefore, cavity modes and field line resonances can be excited with only weak damping when the contrast between the parameters of the two regions is strong.

Since the magnetic fields of Earth and Jupiter are relatively smooth in most regions, the strong gradients needed to provide a strong reflection of these modes mostly occur due to the change in density. The differences between the density structure of the two magnetospheres leads to differences in the types of modes they can support. In the next section of this review, we will discuss the density profiles for the two magnetospheres. Then in subsequent sections, we will discuss field line resonances and cavity mode structures in both magnetospheres. Finally we will introduce a new type of resonant mode that is unique to Jupiter, a shear Alfvén mode resonance in the low density region between the ionosphere and plasma sheet.

**DENSITY STRUCTURE OF THE MAGNETOSPHERES OF EARTH AND JUPITER**

Next, we discuss the density profiles at the two planets, working our way outward from the planet’s surface starting with the ionosphere. The ionosphere at Earth is very well studied through measurements from sounding rockets, radar measurements from the ground and low-Earth orbiting satellites (e.g., Kelley, 1989). The density in the ionosphere generally peaks at densities of \( 10^2 \)–\( 10^6 \) cm\(^{-3} \) at the peak of the F-layer, at about 200 km. There are large variations in these parameters due to sunlit vs dark conditions as well as effects due to magnetic storm activity in the magnetosphere. An empirical model including these variations is the International Reference Ionosphere (IRI; Bilitza et al., 2017; Alken et al., 2021). The ionosphere is largely populated by heavy ions such as O\(^+\) and NO\(^+\), with protons becoming the dominant ion at higher altitudes, above about 1,000 km.

The Jovian ionosphere is much less understood, since the measurement techniques listed in the previous paragraph are not possible. Radio occultation techniques have been used from both Voyager and Galileo, leading to similar densities of \( 10^5 \)–\( 10^6 \) cm\(^{-3} \) (e.g, McConnell et al., 1982; Hinson et al., 1997, 1998), while a more recent study by Mendillo et al. (2022) has indicated that peak densities are at \( 10^5 \) cm\(^{-3} \). Measurements from the Microwave Radiometer instrument on Juno have suggested that even higher densities, up to \( 10^7 \) cm\(^{-3} \) might be present (Hodges et al., 2020). Modeling results (e.g., Millward et al., 2002) are consistent with the lower densities. These results also indicate that at Jupiter, the dominant ion at altitudes below about 1,000 km is H\(^+\), which is an ion that can only exist under dense, cold conditions (e.g., Yelle and Miller, 2004). At higher altitudes, this ion dissociates and protons are the dominant ion.

Recent Juno measurements have provided measurements of the electron density in the topside ionosphere by using electromagnetic wave resonances (e.g., Elliott et al., 2021; Sulaiman et al., 2022). These measurements show that the...
plasma density is frequently below 100 cm$^{-3}$ at radial distances below 2 RJ, and can reach values as low as 10$^{-2}$ cm$^{-3}$. These measurements are supported by direct observations of the low energy plasma by the Juno Auroral Distributions Experiment (JADE) on Juno (Allegrini et al., 2021). Because of the strong Jovian magnetic field, which is the order of 1 G (or 100 $\mu$T) at 2 RJ, the Alfven speed is essentially equal to the speed of light at this and higher altitudes. In the Earth’s auroral zone, the plasma density is also low, with densities less than 1 cm$^{-3}$ at 2 RE where the magnetic field is about 5 $\mu$T, which gives an Alfven speed of about 100,000 km/s or one-third of the speed of light.

Another contrast is that Earth possesses a rather dense plasmasphere, which extends to about 4–6 RE and has densities up to about 1,000 cm$^{-3}$ (e.g., Gallagher et al., 2000, 2021). The plasmaspheric mass density can also be determined by considering the frequency of field line resonances, a research area known as magnetoseismology (e.g., Takahashi and Anderson, 1992; Denton, 2006; Waters et al., 2006), which confirms these densities. The plasmasphere often has a rather sharp edge, the plasmapause, that can act to reflect fast mode waves (as described above), forming cavity mode resonances in the plasmasphere (Waters et al., 2002; Takahashi et al., 2018), sometimes called virtual resonances since the plasmapause is not a perfect reflector (Lee, 1998). A density model for the dipole regions of Earth’s magnetosphere is given in Figure 1. In contrast, a similar plasmasphere is not present at Jupiter, likely due to the rapid rotation of the planet and the inner magnetosphere. The centrifugal acceleration overcomes the gravitational acceleration at Jupiter at radial distances greater than 2.24 RJ (e.g., Ray et al., 2009), and so a stable, corotating plasmasphere such as is found at Earth does not seem to form at Jupiter.

Moving farther out in the magnetospheres, at Earth the geomagnetic tail contains a plasma sheet that is largely composed of solar wind ions, with a minor fraction consisting of ions accelerated up from the ionosphere. Typical parameters of the central plasma sheet (e.g., Hughes, 1995) are a density of 0.3 cm$^{-3}$ and a magnetic field strength of 10 nT, which gives an Alfven speed of 400 km/s, assuming a hydrogen plasma. This plasma sheet is surrounded by a low-density lobe, with typical parameters of a magnetic field of 20 nT and a density of 0.01 cm$^{-3}$, giving an Alfven speed of about 4,400 km/s. In contrast, Jupiter contains a plasma disk that is largely composed of plasma originating at the moon Io, whose volcanoes emit sulfur and oxygen which is then ionized and transported outward by centrifugal forces (Bagenal and Delamere, 2011). At a radial distance of 20 RJ, this plasma has a density of about 1 cm$^{-3}$ and a magnetic field strength of 20 nT, according to the model of Connerney et al. (1981) (The updated model of Connerney et al., 2020, has a slightly lower field.). This gives an Alfven speed of 100 km/s, assuming an average mass of 16 amu. However, in the case of Jupiter, the lobe regions appear to be very empty, with Alfven speeds approaching the speed of light. Figure 2 (updated from Lysak and Song, 2020) gives the magnetic field, density and Alfven speed for a model based on Bagenal and Delamere (2011) and Connerney et al. (2020).

A final distinction between the two magnetospheres is that the solar wind impacts the Earth’s plasma sheet much more than at Jupiter. Changing solar wind conditions can lead to reconnection occurring at distances of 20 RE during magnetospheric substorms, while reconnection at Jupiter is thought to occur much farther out. Woch et al. (2002) note that the transition between inward (toward Jupiter) and outward flows occurs at distances greater than 70 RJ. Thus, the Jovian tail is more likely to be able to support field line resonances at larger radial distances from the planet than at Earth.

**FIELD LINE RESONANCES AND CAVITY MODES AT EARTH**

The study of field line resonances has a long history, starting from the seminal reports of Dungey (1954) and Tamao (1964). This was put on a firm footing by the work of Cummings et al. (1969), who used a dipolar coordinate system to compute the resonant
frequencies of both toroidal modes (with a magnetic perturbation in the azimuthal direction) and poloidal modes (with the magnetic field in the radial direction at the equator). This work was extended by Singer et al. (1981), who included non-dipolar fields with an azimuthal dependence to determine the resonant frequencies as a function of local time.

A major observational advance was made by Samson (1972), who concluded from the polarization of the field-line resonances that they were excited as a result of Kelvin-Helmholtz instability at the magnetopause. This instability leads to the formation of compressional (fast mode) waves that propagate across field lines until they hit a field line whose resonant frequency matches the frequency of the fast mode waves. This resonant point is generally at smaller radial distances than the classical turning point of the fast mode waves, indicating that tunneling from the turning point to the resonant point should occur. The theory of this process was discussed by Zhu and Kivelson (1988) by using a box model in which the field lines are straightened out. Numerical studies of this process in a dipole model were carried out by Lee and Lysak (1989, 1990), who noted that tunneling was not necessary in the dipole model due to the curvature of the field lines.

At lower L-shells, field line resonances have often been used to determine the plasma mass density, an area called magnetoseismology. For example, Takahashi and Anderson (1992) used measurements from the magnetometer aboard the AMPTE CCE satellite to determine the inferred density and Alfvén speed within the $L = 7$ L shell. These observations clearly show FLRs with frequencies of a few tens of millihertz, with a jump in the frequencies at $L = 4$ to 5, indicating the presence of the plasmapause. Denton et al. (2006) generalized the plasma density model used in previous studies, which assumed a power law distribution of density, by using observations of multiple FLR harmonics to fit to a polynomial distribution of the density. They found that at L shells of 6–8, while the electron density was well fit by a single power law, the mass density distribution had a peak near the equator, which suggested that heavy ions were concentrated near the equator.

Fewer studies have reported on field line resonances at higher L shells. This may be because the tail is frequently disrupted by storm and substorm processes during which the tail is dramatically reconfigured, making a standing resonance more difficult to sustain. Another point is that the FLR frequencies can become very low. There have been a few indications of such low frequency FLRs. Samson et al. (1996) reported FLRs in the 1–3 mHz range at $L = 7$ near midnight local times from ground based observations. Rankin et al. (2000) noted that resonances in this frequency range could be explained by considering the stretched magnetic topology in the midnight region. The most extreme examples of low frequency FLRs in the tail were presented by Zheng et al. (2006), who showed coordinated observations of FLRs from Cluster at 19 RE at about 1.1 mHz, or a period of 15 min together with ground observations on conjugate field lines at the same frequency. These authors also reported FLRs at 2.5 mHz from GOES-12 and Geotail at 9 RE, and Polar at 2 mHz at 10.5 RE as well as at 1.5 mHz at 14 RE. Therefore when conditions permit, field line resonances can be seen throughout the magnetosphere and into the near-Earth magnetotail.

In contrast with the relatively common observations of FLRs in the magnetosphere, cavity mode oscillations have been more difficult to observe. One early example was provided by Kivelson et al. (1984) and Kivelson and Southwood (1986) of global pulsations in the 5–8 min range (2–3 mHz) in the dayside magnetosphere. On the dayside, the plasmapause and the magnetopause provide strong gradients that can act to confine these cavity modes on the dayside. On the other hand, on the nightside, there is no comparable boundary to the magnetopause to confine these modes. In contrast, Samson et al. (1992) have suggested that field line resonances at discrete frequencies of 1.3, 1.9, 2.6 and 3.3 mHz were associated modes propagating in a waveguide formed in the magnetotail. Modeling efforts (Wright, 1994; Keller and Lysak, 2001) have shown the possibility of supporting such modes, but direct observation of the fields in this waveguide have proven elusive. As with the FLRs, this may be because the dynamics of the magnetotail may disrupt for formation of these very long period waves.

On the other hand, the plasmasphere is also capable of supporting cavity modes. Lee (1996) studied the possibility of plasmaspheric cavity modes. He noted that the imperfect reflection of waves at the plasmaspheric boundary suggested

![Figure 2](image.png)
that these modes should be called virtual resonances rather than pure cavity modes. Whatever such modes are called, a recent study by Takahashi et al. (2018) has provided some of the best evidence for the excitation of these oscillations in the dayside magnetosphere in response to the impact of an interplanetary shock using data from the Van Allen Probes mission.

We have examined this event using a ULF wave code set in a dipolar geometry that has been used in a number of previous papers (e.g., Lysak et al., 2013; Lysak et al., 2015; Lysak et al., 2020). This code uses non-orthogonal coordinates to address the differences between a dipolar geometry appropriate to the magnetosphere and the spherical geometry of the ionosphere. The model equations are Maxwell’s equations, coupled with ionospheric currents given by Ohm’s Law. Thus the equations modeled are

\[
\frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E} \quad \varepsilon_\perp \frac{\partial \mathbf{E}_\perp}{\partial t} = \frac{1}{\mu_0} (\nabla \times \mathbf{B})_\perp - \mathbf{J} = \sigma_P \mathbf{E}_\perp - \sigma_H \mathbf{E}_\perp \times \mathbf{b}
\]

Here \(\sigma_P\) and \(\sigma_H\) are the Pedersen and Hall conductivities, respectively, and \(\mathbf{b}\) is the direction of the magnetic field. The permittivity \(\varepsilon_\perp = \varepsilon_0 (1 + c^2 / V_A^2)\) includes the effects of the displacement and polarization currents.

This code was run with a density profile modeled after wave observations by the Van Allen Probes mission. Cavity modes with frequencies of 13 mHz, 30 and 43 mHz were found in the simulation, very close to observed values of 13 mHz, 26 and 40 mHz. Figure 3 (from Takahashi et al., 2018) shows the density profile used in the model (panel a), the spectrum of both the cavity modes (panel b, indicated by the azimuthal, or \(E_\phi\) component of the electric field) and the field line resonances (the \(E_\nu\) component, panel c). It can be seen that the cavity modes are not strictly confined within the plasmasphere. Note that Figure 3A gives the electron density, not the mass density. In the simulations, we assume that the plasmasphere is mainly hydrogen, although it is likely that there is some population of heavy ions. In addition, the simulations have assumed a slightly lower density than the observations to account for the fact that the magnetic field is compressed on the dayside, leading to larger Alfvén speeds.

A final type of resonant cavity is the topside ionosphere, which supports modes in what has been called the Ionospheric Alfvén...
MODES AT JUPITER

Given the larger size of Jupiter’s magnetosphere, one might expect that field line resonances at Jupiter would occur at lower frequencies than at Earth. This remains true despite the fact that the magnetic field is stronger at Jupiter while densities are not that much different than on Earth, leading to larger Alfvén speeds. The best evidence for field line resonances at Jupiter are the so-called Quasi-Periodic Oscillations with periods of 10–60 min that have been observed in the aurora by the Hubble Space Telescope (Nichols et al., 2017) and by the Japanese Subaru satellite (Watanabe et al., 2018) in the infrared. Observations from Voyager 2 have also shown magnetic fluctuations in this period range (Khurana and Kivelson, 1989). Similar observations from Galileo have been reported by Wilson and Dougherty (2000). A detailed study of these oscillations was done by Manners et al. (2018), Manners and Masters (2019), and Manners and Masters (2020). Manners and Masters (2019) used a box model to analyze these observations, and showed that there are maxima in the power in the transverse magnetic fields at periods of about 22, 14, 7 and 4 min at a radial distance of 23 RJ. In the box model used in this work, these oscillations corresponded to the first, third, seventh and 11th harmonics of the field line resonance. In particular, all of these modes have antinodes in the magnetic field at the equator, indicative of the driving source.

These observations were tested in a more realistic magnetosphere by Lysak and Song (2020). As shown above in Figure 2, we used the magnetic field model of Connerney et al. (1981) and the plasma model of Bagenal and Delamere (2011). We then performed an eigenvalue analysis to determine the resonant frequencies and a time-domain simulation for the M = 23 field line (where M refers to the distance of the equatorial crossing, in Jovian radii) to confirm the mode structure of these waves. These frequencies and the corresponding period (in minutes) are shown in Figure 4 (Lysak and Song, 2020). We found a rich set of frequencies in the 10–40 min range could be supported by the model. The modes observed by Manners and Masters (2019) here corresponded to modes 6, 10, 18, and 32, with periods of 22.4, 13.0, 7.1 and 3.9 min, respectively (here we are counting the fundamental as mode 1, with the first harmonic being mode 2, and so on). The time domain simulations supported the idea that these harmonics could be excited by a bipolar pulse in the electric field, corresponding to a shear flow in the magnetotail. Such sheared flows might be expected in this region of the Jovian magnetosphere where the co-rotation of the plasma with the planet is breaking down. As this break down is associated with the generation of auroral field-aligned currents, these waves could potentially produced the observed oscillations in the aurora.

Manners and Masters (2020) investigated the local time dependence of ULF waves in the Jovian magnetosphere, including compressional waves (fast mode) as well as transverse waves (Alfvén mode). The two modes were observed in the range of periods from 10 to 60 min, with periods of 15, 30 and 40 min being dominant. The distribution of the waves were similar in the noon and midnight sectors, suggesting that the compressional waves were ducted through the plasma disk from a dayside source to the nightside. However, they observed greater wave power within 10 RJ than at radial distances of greater than 40 RJ, suggesting that the source of these waves was internal rather than imposed from the magnetopause by, for example, dynamic pressure pulses in the solar wind or by Kelvin-Helmholtz instabilities.

One obvious possibility for an internal source is the motion of the moon Io (and to a lesser extent, Ganymede and Europa) through the magnetosphere (or more precisely, by the motion of the co-rotating plasma past the moon). It has long been known that this interaction gives rise to “Alfvén wings” that couple Io with the ionosphere of Jupiter (e.g., Goertz, 1980; Neubauer, 1980; Acuña et al., 1981; Belcher et al., 1981; Gurnett and Goertz, 1981; Bagenal, 1983; Crary, 1997; Chust et al., 2005; Hinton et al., 2019). While much of this work has focused on transverse Alfvén waves, Glassmeier et al. (1989) observed both transverse and compressional waves in the plasma torus. It seems reasonable that as the co-rotating plasma impacts and is diverted around Io, compressions in the magnetic field would be excited. These waves could be trapped in the Io plasma torus itself (denoted as a “torus resonance” by Manners and Masters (2020)), or could leak out to fill the plasma sheet that forms tailward of the Io plasma torus. As noted above, the dense plasma of heavy ions produced by the Io interaction would lead to strong cavity oscillations. In addition, the ionogenic plasma moves outward under the influence of the centrifugal force. However, this motion is not smooth but rather is in the form of irregular interchange motions that would seem like a natural
source of ULF waves. Further study is clearly needed to investigate these types of cavity modes at Jupiter.

As noted above, there is also a sharp decrease in the plasma density in the topside ionosphere of Jupiter (e.g., Allegrini et al., 2021; Elliott et al., 2021), which should lead to an ionospheric Alfvén resonator at Jupiter. As at Earth, this can produce a broadband acceleration of electrons, which are often the dominant form of electron distribution in the Jovian auroral zone. It is worth noting that the magnetic field strength at Jupiter is an order of magnitude bigger than at Earth while the plasma densities are comparable, so that the Alfvén speed is roughly an order of magnitude larger at Jupiter. However, the scale heights of the ionosphere, which scale with the planetary radius, is also an order of magnitude larger than at Earth, so that the IAR frequencies are comparable. However, at Jupiter, it is a 30 keV electron that travels at about 1 R_J/s. Thus, the Alfvénic acceleration process should produce broadband electrons in this energy range.

However, recent observations from Juno indicate that while broadband electrons are frequently seen on field lines connecting to the main auroral emissions, the corresponding Alfvén waves are often not observed on the same field lines (Mauk et al., 2020). This could be because the acceleration is taking place at altitudes above the spacecraft, or that the broadband acceleration in this

FIGURE 4 | Eigenfrequencies as a function of M-shell for first 12 eigenmodes for the density and Alfvén speed given in Figure 3. (A) Frequencies in mHz; (B) Periods in minutes. Note that the fundamental mode, which has periods greater than 80 min for all values of M, is not shown in panel b (Lysak and Song, 2020).
which may give some support to this suggestion. Sulaiman et al. (2022) where the density is higher, observed in the regions equatorward of the main auroral so this hypothesis is difficult to put to the test. Alfvén waves are observed in the regions equatorward of the main auroral emissions (Sulaiman et al., 2022) where the density is higher, which may give some support to this suggestion. There is a clearer signature of Alfvénic acceleration in the flux tube connected to Io (and probably Ganymede and Europa as well). As noted above, Io provides a strong source for Alfvén wave emissions. Szalay et al. (2018), using Juno observations, have observed both broadband acceleration and Alfvén wave turbulence in this region, suggesting that the IAR may be active on these field lines. Moreover, Szalay et al. (2020) have also observed broadband proton acceleration, consistent with an Alfvénic acceleration process. Thus, while more observations will help to clarify these issues, it appears likely that Alfvénic acceleration is dominant on the Io flux tube.

A new resonant cavity that appears to be unique in the Jovian magnetosphere is what could be called a lobe resonator in the very low density region between the ionosphere and the heavy ion plasma disk. This region has an Alfvén speed that is nearly the speed of light, while the ionosphere and the plasma disk have Alfvén speeds below 1,000 km/s. This makes a strong contrast in Alfvén speeds that leads to strong reflection according to Equation 3. This resonator has a period of a few minutes, intermediate between the seconds of the IAR and the tens of minutes for field line resonances. Evidence for this cavity was presented by Lysak et al. (2021a), who were modeling field lines in the main aurora. However, reflections at the boundary of the plasma disk are particularly important in the Io interaction since these reflections return to the ionosphere, producing the elongated tail observed in the aurora. This tail consists of multiple spots when observed with high resolution (e.g., Mura et al., 2018; Moirano et al., 2021). Figure 5 shows a snapshot of a simulation we did (Lysak et al., 2021b) of the Io plasma interaction. This plot shows $E_{\perp}$, the component of the perpendicular electric field that points radially outward near the equator and poleward near the poles, with green and yellow colors indicating radially outward fields and blue and violet being inward. In this run, the source due to Io has been moving across the system, generating Alfvén waves. At this longitude, Io is at its maximum magnetic latitude of about 10°. The contrast in the angle of the field patterns between the low Alfvén speed disk, which covers roughly from −10° to 20° latitude in the figure, and the lobe region of high Alfvén speed can be observed. It can also be seen that the electric fields reverse on each bounce from the disk, consistent with Equation 3 since in this case, $V_2 < V_1$. Understanding this resonant cavity will be key to determining the structure of the Io auroral tail as well as the interaction of other moons with the Jovian magnetosphere.

**SUMMARY AND CONCLUSION**

The theories and observations presented here show that resonant Alfvén wave structures, whether field line resonances for the shear Alfvén mode or cavity resonances for the fast mode, are ubiquitous in the magnetospheres of Earth and Jupiter, and no doubt in other planetary magnetospheres as well. To summarize the results of the papers covered in this review:

1. The magnetospheres of both Earth and Jupiter can support field line resonances consisting of shear Alfvén waves propagating from one ionosphere to the conjugate ionosphere. At Earth, these resonances have periods of minutes, while at Jupiter the periods are tens of minutes.
2. At Earth, the plasmasphere can support cavity modes, also with periods of a few minutes. Coupling between these cavity modes and the field line resonances are important in the dynamics of the magnetosphere. In contrast, at Jupiter, there is not a well defined plasmasphere, so this type of mode cannot exist.
3. On the other hand, Jupiter has a plasma disk consisting of heavy ions due to plasma originating at the moon Io. This disk can support cavity modes with periods of tens of minutes and could couple to the field line resonances at similar frequencies as well. At Earth, there do not seem to be many observations of such resonances in the tail plasma sheet. This is perhaps due to the fact that the geomagnetic tail is often disrupted by substorm dynamics.
4. The magnetospheres of both planets can support an ionospheric Alfvén resonator due to the rapid decrease of density above the ionosphere. These resonances have periods of seconds in both cases, and can contribute to the broadband acceleration of electrons and ions associated with the Alfvénic aurora. In the case of Jupiter, this acceleration is particularly important in the interaction of Io with the co-rotating plasma.
5. At Jupiter, there is also a lobe resonator in the high Alfvén speed region between the ionosphere and the plasma disk, with periods of minutes. This resonator affects the Alfvénic interaction between Io and Jupiter, and leads to the extended auroral tail that is initiated on the Io flux tube. This type of resonator does not appear to be active at Earth.

In conclusion, these various interactions due to the inhomogeneous Alfvén speed play an important role in the short time dynamics of the magnetospheres of Earth and Jupiter. Understanding these interactions will lead to greater understanding of the formation of aurora and the acceleration of particles at these magnetospheres as well as those of other planets, both within our Solar System and in other systems.

**AUTHOR CONTRIBUTIONS**

RL is the sole author of this paper and is solely responsible for its content.

**REFERENCES**

Acuta, M. H., Neuberger, F. M., and Ness, N. F. (1981). Standing Alfvén Wave Current System at Io - Voyager 1 Observations. *J. Geophys. Res.* 86 (A10), 8513–8521. doi:10.1029/JA086iA10p08513

Allen, P., Thebault, E., and Zhou, B. (2021). International Geomagnetic Reference Field: the Thirteenth Generation. *Earth, Planets and Space* 73 (1), 1–25. doi:10.1186/s40623-020-01313-2

Allegrini, F., Kurth, W. S., Elliott, S. S., Saur, J., Livadiotis, G., Nicolaou, G., et al. (2021). Electron Partial Density and Temperature over Jupiter Using Juno Observations. *JGR Space Phys.* 126, 2021JA029426. doi:10.1029/2021JA029426

Bagental, F. (1983). Alfvén Wave Propagation in the Io Plasma Torus. *J. Geophys. Res.* 88 (A4), 3013–3025. doi:10.1029/JA088iA04p03013

Bagental, F., and Delamere, P. A. (2011). Flow of Mass and Energy in the Magnetospheres of Jupiter and Saturn. *J. Geophys. Res.* 116, A05209. doi:10.1029/2010JA016294

Bilitza, D., Alladiil, D., Truhlik, V., Shubin, V., Galkin, I., Reinisch, B., et al. (2017). International Reference Ionosphere 2016: From Ionospheric Climate to Real-time Weather Predictions. *Space weather*. 15 (2), 418–429. doi:10.10202016so159

Chaston, C. C., Bonnell, J. W., Carlson, C. W., Berthomier, M., PetiolasRoth, L. M. I., et al. (2002). Electron Acceleration in the Ionospheric Alféven Resonator. *J. Geophys. Res.* 107 (A11), 1413. doi:10.1029/2002JA009272

Chaston, C. C., Petiolas, L. M., Bonnell, J. W., Carlson, C. W., Ergun, R. E., McFadden, J. P., et al. (2003). Width and Brightness of Auroral Arcs Driven by Inertial Alfvén Waves. *J. Geophys. Res.* 108 (A2), 1091. doi:10.1029/2001JA007537

Chen, L., and Hasegawa, A. (1974). A Theory of Long-Period Magnetic Pulsations: 1. Steady State Excitation of Field Line Resonance. *J. Geophys. Res.* 79, 1024–1032. doi:10.1029/JA079i007p01024

Chust, T., Roux, A., Kurth, W. S., Gurnett, D. A., Kivelson, M. G., and Khurana, K. K. (2005). Are Io’s Alfvén Wings Filamented? Galileo Observations. *Pluto. Space Sci.* 53 (4), 395–412. doi:10.1151/ps.2004.09.021

Connerney, J. E. P., Acuña, M. H., and Ness, N. F. (1981). Modeling the Jovian Current Sheet and Inner Magnetosphere. *J. Geophys. Res.* 86, 8370–8384. doi:10.1029/ja086iA10p08370

Connerney, J. E. P., Timmins, S., Herceg, M., and Jorgensen, J. L. (2020). A Jovian Magnetodisc Model for the Juno Era. *J. Geophys. Res. Space Phys.* 125, e2020JA028138. doi:10.1029/2020JA028138

**FUNDING**

The research behind this research has been supported by a National Science Foundation grant AGS-1840891 and a National Aeronautical and Space Administration grant 80NSSC20K1269. Computing support has been provided by the Minnesota Supercomputer Institute.

**ACKNOWLEDGMENTS**

This work has benefited from numerous conversations with colleagues both with regard to the Earth-based and Jupiter-based aspects of the work. In particular, I acknowledge contributions from Yan Song and Sadie Elliott (University of Minnesota), Colin Waters and Murray Sciffer (Newcastle University, Australia), Kazue Takahashi and Barry Mauk (Johns Hopkins University Applied Physics Lab), Ali Sulaiman and Bill Kurth (University of Iowa), Fran Bagental (University of Colorado), and H. Arthur Manners and Adam Masters (Imperial College London).

Crary, F. J. (1997). On the Generation of an Electron Beam by Io. *J. Geophys. Res. Space Phys.* 102, 37.

Cummings, W. D., O’Sullivan, R. J., and Coleman, P. J. (1969). Standing Alfvén Waves in the Magnetosphere. *J. Geophys. Res.* 74, 778–793. doi:10.1029/ja074i003p00778

Denton, R. E., Takahashi, K., Gulkis, I. A., Nueami, P. A., Huang, X., Reinisch, B. W., et al. (2006). Distribution of Density along Magnetospheric Field Lines. *J. Geophys. Res.* 111, A04213. doi:10.1029/2005JA011414

Dunse, J. W. (1954). Electrodymanics of the Upper Atmosphere. in *Ionospheric Research Laboratory Scientific Report, 69.* PA: Penn State University Press, University Park.

Elliott, S. S., Garnett, D. A., Kurth, W. S., Mauk, B. H., Ebert, R. W., Clark, G., et al. (2018). The Acceleration of Electrons to High Energies over the Jovian Polar Cap via Whistler Mode Wave-Particle Interactions. *J. Geophys. Res. Space Phys.* 123, 7523–7523. doi:10.1029/2018JA025797

Elliott, S. S., Sulaiman, A. H., Kurth, W. S., Faden, J., Allegrini, F., Valek, P., et al. (2021). The High-Latitude Extension of Jupiter’s Io Torus: Electron Densities Measured by Juno Waves. *J. Geophys. Res. Space Phys.* 126, e2021JA029195. doi:10.1029/2021JA029195

Gallagher, D. L., Comfort, R. H., Katus, R. M., Sandel, B. R., Fung, S. F., and Adrian, M. L. (2021). The Breathing Plasmasphere: Erosion and Refilling. *J. Geophys. Res. Space Phys.* 126, e2020JA028727. doi:10.1029/2020JA028727

Gallagher, D. L., Craven, P. D., and Comfort, R. H. (2000). Global Core Plasma Model. *J. Geophys. Res.* 105, 18819–18833. doi:10.1029/1999ja0090241

Glassmeier, K.-H., Hoensm, M., and Untiedt, J. (1989). Ground-based and Satellite Observations of Traveling Magnetospheric Convection Twin-Vortices. *J. Geophys. Res.* 94, 2520.

Goertz, C. (1980). Io’s Interaction with the Plasma Torus. *J. Geophys. Res.* 85, 2949–2956.

Garnett, D. A., and Goertz, C. K. (1981). Multiple Alfvén Wave Reflections Excited by Io: Origin of the Jovician Demicentric Arcs. *J. Geophys. Res.* 86 (A2), 717–722. doi:10.1029/JA086iA02p00717

Hinson, D. P., Flasar, F. M., Kliore, A. J., Schinder, P. J., Twicken, J. D., and Herrera, R. G. (1997). Jupiter’s Ionosphere: Results from the First Galileo Radio Occultation Experiment. *Geophys. Res. Lett.* 24, 2107–2110. doi:10.1029/97GL01608

Hinson, D. P., Twicken, J. D., and Karayel, E. T. (1998). Jupiter’s Ionosphere: New Results from Voyager 2 Radio Occultation Measurements. *J. Geophys. Res.* 103, 9505–9520. doi:10.1029/97ja03689
Hinton, P. C., Bagena, F., and Bonfond, B. (2019). Alfven Wave Propagation in the Io Plasma Torus. Geophys. Res. Lett. 46, 1242–1249. doi:10.1029/2018GL081472

Hodges, A., Steffes, P., Bellotti, A., Waite, J. H., Brown, S., Oyafuso, F., et al. (2020). Observations and Electron Density Retrievals of Jupiter’s Discrete Auroral Arcs Using the Juno Microwave Radiometer. J. Geophys. Res. Space Phys. 125, e2019Je006293. doi:10.1029/2019je006293

Hughes, W. J. (1995). "The Magnetopause, Magnetic, and Magnetic Reconnection," in Introduction to Space Physics. Editors M. G. Kivelson, and C. T. Russell (Cambridge, UK: Cambridge University Press), 227–287. doi:10.1017/9781139878296.010

Keller, K. A., and Lysak, R. L. (2001). MHD Simulation of Magnetospheric Waveguide Modes. J. Geophys. Res. 106, 8447.

Kelley, M. C. (1989). The Earth’s Ionosphere. Academic Press.

Kivelson, M. G. (1995). “Pulsations and Magnetohydrodynamic Waves,” in Introduction to Space Physics. Editors M. G. Kivelson, and C. T. Russell (Cambridge, UK: Cambridge University Press), 330–355. doi:10.1017/9781139878296.012

Kivelson, M. G., and Southwood, D. J. (1986). Coupling of Global Magnetospheric MHD Eigenmodes to Field Line Resonances. J. Geophys. Res. 91, 4345.

Kivelson, M. G., Etcheto, J., and Trotignon, J. G. (1984). Global Compressional Oscillations of the Terrestrial Magnetosphere: The Evidence and a Model. J. Geophys. Res. 89, 9851.

Khurana, K., and Kivelson, M. G. (1989). Ultralow Frequency MHD Waves in Jupiter’s Middle Magnetosphere. J. Geophys. Res. 94, 5241.

Lee, D.-H. (1998). On the Generation Mechanism of Pi 2 Pulsations in the Earth’s Polar Cap and Main Aurora: A Broad Overview. J. Geophys. Res. Space Phys. 125, e2019Ja027699. doi:10.1029/2019Ja027699

McConnell, J. C., Holberg, J. B., Smith, G. R., Sandel, B. R., Shemansky, D. E., and Broadfoot, A. L. (1982). A New Look at the Ionosphere of Jupiter in Light of the UVS Occultation Results. Planet. Space Sci. 30, 151–167. doi:10.1016/0032-0633(82)90086-1

Mendillo, M., Narvaez, C., Moore, L., and Withers, P. (2022). Jupiter’s Enigmatic Ionosphere: Electron Density Profiles from the Pioneer, Voyager, and Galileo Radio Occultation Experiments. J. Geophys. Res. Planets 127, e2021Je007169. doi:10.1029/2021je007169

Menk, F. W., and Waters, C. L. (2013). Magnetoseismology. Weinheim, Germany: Wiley VCH.

Millward, G., Miller, S., Stallard, T., Aylward, A. D., and Achilleos, N. (2002). On the Dynamics of the Jovian Ionosphere and Thermosphere III. The Modelling of Auroral Conduction. Icarus 160, 95–107. doi:10.1006/icar.2002.6951

Moirano, A., Mura, A., Adriani, A., Dols, V., Bonfond, B., Waite, J. H., et al. (2021). Morphology of the Auroral Tail of Io, Europa, and Ganymede from IRAM L-Band Imager. J. Geophys. Res. Space Phys. 126, e2021Ja029450. doi:10.1029/2021Ja029450

Mura, A., Adriani, A., Connerney, J. E. P., Bolton, S., Altieri, F., Bagena, F., et al. (2018). Juno Observations of Spot Structures and a Split Tail in Io-Induced Aurorae on Jupiter. Science 361, 774–777. doi:10.1126/science.aat1450

Nichols, J. D., Yeoman, T. K., Bunce, E. J., Chowdhury, M. N., Cowley, S. W. H., and Robinson, T. R. (2017). Periodic Emission within Jupiter’s Main Auroral Oval. Geophys. Res. Lett. 44, 9192–9198. doi:10.1002/2017GL074824

Polyakov, S. V., and Rapoport, V. O. (1981). Ionospheric Alfvén Resonator, Geomag. Aeronoy 21, 816.

Rankin, R., Fenrich, F., and Tikhonov, V. T. (2000). Shear Alfvén Waves on Stretched Magnetic Field Lines Near Midnight in Earth’s Magnetosphere. Geophys. Res. Lett. 27, 3265.

Ray, L. C., Su, Y.-J., Ergun, R. E., Delamar, P. A., and Bagenal, F. (2009). Current-voltage Relation of a Centrifuigally Confined Plasma. J. Geophys. Res. 114, a–n. doi:10.1029/2008Ja015969

Samson, J. C. (1972). Three-dimensional Polarization Characteristics of High-Latitude Pi5 Geomagnetic Micropulsations. J. Geophys. Res. 77, 6145.

Samson, J. C., Harrold, R. G., Rouhoniemi, J. M., Greenwald, R. A., and Walker, A. D. M. (1992). Field Line Resonances Associated with MHD Waveguides in the Magnetosphere. Geophys. Res. Lett. 19, 441.

Samson, J. C., Cogger, L. L., and Pao, Q. (1996). Observations of Field Line Resonances, Auroral Arcs, and Auroral Vortex Structures. J. Geophys. Res. 101, 373.

Singer, H. J., Southwood, D. J., Walker, R. J., and Kivelson, M. G. (1982). Alfven Wave Resonances in a Realistic Magnetospheric Magnetic Field Geometry. J. Geophys. Res. 86, 4589–4596. doi:10.1029/ja086i06a004589

Southwood, D. J. (1974). Some Features of Field Line Resonances in the Magnetosphere. Planet. Space Sci. 22, 483–491. doi:10.1016/0032-0633(74)90078-6

Stix, T. H. (1992). Waves in Plasmas. Berlin: Springer.

Sulaiman, A. H., Allegren, F., Clark, G., Gladstone, G. R., Kotsiaros, S., Kurtz, W. S., et al. (2022). Jupiter’s Low-altitude Auroral Zones: Fields, Particles, Plasma Waves, and Density Depletions. J. Geophys. Res. Space Phys. submitted to.

Szalay, J. R., Bonfond, B., Allegren, F., Bagena, G., Bagenal, F., Bolton, S., Clark, G., et al. (2018). In situ Observations Connected to the Io Footprint Tail Aurora. J. Geophys. Res. Planets 123, 3061. doi:10.1029/2018je005752

Takahashi, K., and Anderson, B. J. (1992). Distribution Of ULF Energy (< 80 MHz) In The Inner Magnetosphere: A Statistical Analysis Of AMPTE CCE Magnetic Field Data. J. Geophys. Res. 97 (10), 751. doi:10.1029/92Ja000328

Takahashi, K., Lysak, R., Vellante, M., Kletzing, C. A., Hartinger, M. D., and Smith, C. W. (2018). Observation and Numerical Simulation of Cavity Mode Oscillations Excited by an Interplanetary Shock. J. Geophys. Res. Space Phys. 123. doi:10.1002/2017ja026439

Tamao, T. (1964). The Structure of Three-Dimensional Hydromagnetic Waves in a Uniform Cold Plasma. J. Geomagn. Geoelec. 16, 89–114. doi:10.5636/ijg.16.89

Watanabe, H., Kita, H., Tao, C., Kagitani, M., Sakanoi, T., and Kasaba, Y. (2018). Pulsation Characteristics of Jovian Infrared Northern Aurora Observed by the Subaru IRCS with Adaptive Optics. Geophys. Res. Lett. 45. doi:10.1029/2018Gl079411
Waters, C. L., Kabin, K., Rankin, R., Donovan, E., and Samson, J. C. (2007). Effects of the Magnetic Field Model and Wave Polarisation on the Estimation of Proton Number Densities in the Magnetosphere Using Field Line Resonances. *Planet. Space Sci.* 55, 809–819. doi:10.1016/j.pss.2006.04.041

Waters, C. L., Takahashi, K., Lee, D.-H., and Anderson, B. J. (2002). Detection of Ultralow-Frequency Cavity Modes Using Spacecraft Data. *J. Geophys. Res.* 107 (A10), 1284. doi:10.1029/2001JA000224

Wilson, R. J., and Dougherty, M. K. (2000). Evidence provided by Galileo of Ultra Low Frequency Waves within Jupiter’s Middle Magnetosphere. *Geophys. Res. Lett.* 27, 835.

Woch, J., Krupp, N., and Legg, A. (2002). Particle Bursts in the Jovian Magnetosphere: Evidence for a Near-Jupiter Neutral Line. *Geophys. Res. Lett.* 29, 1138. doi:10.1029/2001GL014080

Wright, A. N. (1994). Dispersion and Wave Coupling in Inhomogeneous MHD Waveguides. *J. Geophys. Res.* 99, 159.

Yelle, R. V., and Miller, S. (2004). "Jupiter’s Thermosphere and Ionosphere," in *Jupiter: The Planet, Satellites, and Magnetosphere*. Editors F. Bagenal, T. Dowling, and W. McKinnon (Cambridge, UK: Cambridge University Press), 185.

Zheng, Y., Lui, A. T. Y., Mann, I. R., Takahashi, K., Watermann, J., Chen, S.-H., et al. (2006). Coordinated Observation of Field Line Resonance in the Mid-tail. *Ann. Geophys.* 24, 707.

Zhu, X. M., and Kivelson, M. G. (1988). Analytic Formulation and Quantitative Solutions of the Coupled ULF Wave Problem. *J. Geophys. Res.* 93, 8602.

**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

The handling editor KT declared a shared group NSF with the author at the time of review.

**Publisher’s Note:** All claims expressed in this article are solely those of the authors and do not necessarily represent those of their affiliated organizations, or those of the publisher, the editors and the reviewers. Any product that may be evaluated in this article, or claim that may be made by its manufacturer, is not guarantied or endorsed by the publisher.

Copyright © 2022 Lysak. This is an open-access article distributed under the terms of the Creative Commons Attribution License (CC BY). The use, distribution or reproduction in other forums is permitted, provided the original author(s) and the copyright owner(s) are credited and that the original publication in this journal is cited, in accordance with accepted academic practice. No use, distribution or reproduction is permitted which does not comply with these terms.