Quantification of CH$_4$ emissions from waste disposal sites near the city of Madrid using ground- and space-based observations of COCCON, TROPOMI and IASI

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**Abstract.** The objective of this study is to derive methane (CH$_4$) emissions from three landfills, which are found to be the most significant CH$_4$ sources in the metropolitan area of Madrid in Spain. We derive CH$_4$ emissions from the CH$_4$ enhancements observed by spaceborne and ground-based instruments. We apply satellite-based measurements from the TROPOspheric Monitoring Instrument (TROPOMI) and the Infrared Atmospheric Sounding Interferometer (IASI) together with measurements from the ground-based COllaborative Carbon Column Observing Network (COCCON) instruments.

In 2018, a 2-week field campaign for measuring the atmospheric concentrations of greenhouse gases was performed in Madrid in the framework of Monitoring of the Greenhouse Gases Concentrations in Madrid (MEGEIMAD) project. Five COCCON instruments were deployed at different locations around the Madrid city center, enabling the observation of total column-averaged CH$_4$ mixing ratios (XCH$_4$). Considering the prevalent wind regimes, we calculate the wind-assigned XCH$_4$ anomalies for two opposite wind directions. Pronounced bipolar plumes are found when applying the method to NO$_2$, which implies that our method of wind-assigned anomaly is suitable to estimate enhancements of trace gases at the urban level from satellite-based measurements. For quantifying the CH$_4$ emissions, the wind-assigned plume method is applied to the TROPOMI XCH$_4$ and to the lower tropospheric CH$_4$/dry-air column ratio (TXCH$_4$) of the combined TROPOMI+IASI product.

As CH$_4$ emission strength we estimate $7.4 \times 10^{25} \pm 6.4 \times 10^{24}$ molec. s$^{-1}$ from the TROPOMI XCH$_4$ data and $7.1 \times 10^{25} \pm 1.0 \times 10^{25}$ molec. s$^{-1}$ from the TROPOMI+IASI merged TXCH$_4$ data. We use COCCON observations to estimate the local source strength as an independent method. COCCON observations indicate a...
weaker CH$_4$ emission strength of 3.7 $\times$ 10$^{25}$ molec. s$^{-1}$ from a local source (the Valdemingómez waste plant) based on observations from a single day. This strength is lower than the one derived from the satellite observations, and it is a plausible result. This is because the analysis of the satellite data refers to a larger area, covering further emission sources in the study region, whereas the signal observed by COCCON is generated by a nearby local source. All emission rates estimated from the different observations are significantly larger than the emission rates provided via the official Spanish Register of Emissions and Pollutant Sources.

1 Introduction

Methane (CH$_4$) is the second most important anthropogenic greenhouse gas (GHG) after carbon dioxide (CO$_2$) and contributes about 23.4% to the radiative forcing by long-lived GHGs in the atmosphere (Etminan et al., 2016). The amount of atmospheric CH$_4$ has increased 260% with respect to pre-industrial levels, reaching 1877 ppb in 2019 (World Meteorological Organization, 2020). The global atmospheric CH$_4$ emissions are approximately 40% caused by natural sources (e.g., wetlands and termites), and about 60% of emissions are from anthropogenic sources (Saunois et al., 2020). The anthropogenic sources of CH$_4$ mainly originate from production and burning of fossil fuels, ruminant animals, agriculture and waste management (Bousquet et al., 2006; Chynoweth et al., 2010; Saunois et al., 2020). The waste management sector accounts for 21.5% of the total anthropogenic CH$_4$ emissions (Crippa et al., 2019), in which ~44% of emissions are from landfills. The global uncertainty share of landfills is about 55% (Solazzo et al., 2021). The metropolitan cities are continuously growing due to population movements, industries, etc., and, thus, more and more cities incorporate landfills (and other potential CH$_4$ sources) into their limits and influential areas, making landfills become one of the main CH$_4$ sources. Since CH$_4$ emissions from landfills can vary over several orders of magnitude due to different factors, e.g., the texture and thickness of cover soils, as well as seasonal climate, they become complex sources (Cambaliza et al., 2015). Therefore, the quantification of CH$_4$ emission from landfills using spaceborne and ground-based observations is of importance for future climate emission scenarios and for monitoring changes in emissions.

Many studies have demonstrated the capabilities of satellite observations to estimate CH$_4$ emissions, e.g., from oil and gas sector, including accidental leakages (e.g., Pandey et al., 2019; Varon et al., 2019; De Gouw et al., 2020; Schneider et al., 2020). Satellite retrievals using thermal infrared nadir spectra as observed by IASI (Infrared Atmospheric Sounding Interferometer) or TES (Tropospheric Emission Spectrometer) are especially sensitive to CH$_4$ concentrations between the middle troposphere and the stratosphere (e.g., Siddans et al., 2017; García et al., 2018; De Wachter et al., 2017; Kulawik et al., 2021; Schneider et al., 2021a). Schneider et al. (2021a) developed an a posteriori method for combining the TROPOMI and IASI products to detect tropospheric CH$_4$, which has a positive bias of ~1% with respect to the reference data. The Total Carbon Column Observing Network (TCCON), a network of high-resolution Fourier-transform infrared spectroscopy (FTIR) spectrometers (Washenfelder et al., 2006), has been designed to provide accurate and long-lasting time series of column-averaged dry-air molar fractions of GHGs and other atmospheric constituents (Wunch et al., 2011). Recently, TCCON GHG observations have been extended by the COllaborative Carbon Column Observing Network (COCCON, Frey et al., 2019), which is a research infrastructure using well-calibrated low-resolution FTIR spectrometers (Bruker EM27/SUN, Gisi et al., 2012) and a common data analysis scheme. Due to the ruggedness of the portable devices used and simple operability, COCCON is well suited for implementing arrays of spectrometers in metropolitan areas for the quantification of local GHG sources (Hase et al., 2015; Luther et al., 2019; Vogel et al., 2019; Dietrich et al., 2021).

Madrid, Spain, is one of the biggest cities in Europe and has almost 3.3 million inhabitants, with a metropolitan area population of approximately 6.5 million. Thus, the waste is one of the main CH$_4$ emission sources. To measure atmospheric concentrations of GHGs in this urban environment, a 2-week campaign was carried out in the framework of the Monitoring of the Greenhouse Gases Concentrations in Madrid (MEGEI-MAD) project (García et al., 2019) from 24 September to 7 October 2018 in Madrid.

In this study we analyze nearly 3 years of TROPOMI total column-averaged dry-air molar fraction of CH$_4$ (XCH$_4$) measurements, TROPOMI+IASI TXCH4 measurements together with COCCON spectrometer observations made during the MEGEI-MAD campaign, in an attempt to quantify the CH$_4$ emissions from major emission sources – namely three landfills in Madrid, the most important metropolitan area of Spain. In Sect. 2 our methodology is described, which is as follows: we calculate the difference of the satellite data
maps for two opposite wind regimes (we refer to the resulting signals as wind-assigned anomalies). A simple plume model is then applied to predict the wind-assigned anomalies for a chosen position and strength of a source. The results of our study are presented and discussed in Sect. 3, and the conclusions from these results are given in Sect. 4.

2 Method

2.1 Ground-based and spaceborne instrumentations

2.1.1 COCCON XCH$_4$ data set

The Bruker EM27/SUN is a robust and portable FTIR spectrometer, operating at a medium spectral resolution of 0.5 cm$^{-1}$. The EM27/SUN FTIR spectrometer has been developed by the Karlsruhe Institute of Technology (KIT) in cooperation with Bruker Optics GmbH for measuring GHG concentrations (Gisi et al., 2012; Hase et al., 2016). An InGaAs (indium gallium arsenide) photodetector is used as the primary detector, covering a spectral range of 5500–11 000 cm$^{-1}$. A decoupling mirror reflects 40% of the incoming converging beam to an extended InGaAs photodetector element, covering the spectral range of 4000–5500 cm$^{-1}$ for simultaneous carbon monoxide (CO) observations. The recording time, for a typical measurement consisting of five forward and five backward scans, is about 58 s in total.

Several successful field campaigns and long-term deployments have demonstrated that the Bruker EM27/SUN FTIR spectrometer is an excellent instrument with good quality, robustness and reliability, and its performance offers the potential to support TCCON (Frey et al., 2015, 2019; Klappenbach et al., 2015; Chen et al., 2016; Butz et al., 2017; Sha et al., 2020; Jacobs et al., 2020; Tu et al., 2020a, b; Dietrich et al., 2021). The Bruker EM27/SUN spectrometers have become commercially available from April 2014 onwards, and currently about 70 spectrometers are operated by different working groups in Germany, France, Spain, Finland, Romania, USA, Canada, UK, India, Korea, Botswana, Japan, China, Mexico, Brazil, Australia and New Zealand. The development of the COCCON (https://www.imk-asf.kit.edu/english/COCCON.php, last access: 22 December 2020) became possible by continued European Space Agency (ESA) support. COCCON intends to become a supporting infrastructure for GHG measurements based on common standards and data analysis procedures for the EM27/SUN (Frey et al., 2019).

All the Bruker EM27/SUN spectrometers used in the MEGEI-MAD project were operated in accordance with COCCON requirements. The resulting XCH$_4$ data used in this work were generated by the central facility operated by KIT for demonstrating a centralized data retrieval for the COCCON network. For these reasons, we refer to the Bruker EM27/SUN spectrometers as COCCON spectrometers in the following. The COCCON XCH$_4$ data product is derived from the co-observed total column amounts of CH$_4$ and oxygen (O$_2$), and the assumed dry-air molar fraction of O$_2$ (0.2095) (Wunch et al., 2015):

$$XCH_4 = \frac{\text{column}_{CH_4}}{\text{column}_{O_2}} \times 0.2095.$$  

(1)

2.1.2 TROPOMI XCH$_4$ data set

The TROPOMI data processing deploys the RemoTeC algorithm (Butz et al., 2009, 2011; Hasekamp and Butz, 2008) to retrieve XCH$_4$ from TROPOMI measurements of sunlight backscattered by the Earth’s surface and atmosphere in the near-infrared (NIR) and shortwave-infrared (SWIR) spectral bands (Hu et al., 2016, 2018; Hasekamp et al., 2021; Landgraf et al., 2019). This algorithm has been extensively used to derive CH$_4$ and CO$_2$ from GOSAT (Butz et al., 2011; Guerlet et al., 2013). The TROPOMI XCH$_4$ is calculated from the CH$_4$ vertical sub-columns $x_i$ and the dry-air column. The dry-air column is obtained from the surface pressure from the European Centre for Medium-Range Weather Forecasts (ECMWF) and from the altitude from the Shuttle Radar Topography Mission (SRTM) (Farr et al., 2007) digital elevation map with a resolution of 15 arcsec (Lorente et al., 2021a):

$$XCH_4 = \sum_{i=0}^{n} \frac{x_i}{\text{column}_{\text{dry air}}}.$$  

(2)

This study uses the TROPOMI data set of XCH$_4$ from Lorente et al. (2021a), for which an updated retrieval algorithm was implemented to obtain a data set with less scatter. This updated XCH$_4$ has been demonstrated to be in good agreement with TCCON ($-3.4 \pm 5.6$ ppb) and GOSAT ($-10.3 \pm 16.8$ ppb), with a bias and precision below 1%. Here the TROPOMI XCH$_4$ between 30 April 2018 and 30 December 2020 within the rectangular area of 39.5–41.5° N and 4.5–3.0° W (125 km × 220 km) over Madrid is analyzed. In addition, we apply strict quality control to TROPOMI XCH$_4$ (quality value $q = 1.0$) to exclude data of questionable quality and to assure data under clear-sky and low-cloud atmospheric conditions (Lorente et al., 2021a).

2.1.3 IASI CH$_4$ data and their synergetic combination with TROPOMI data

The IASI sensors are currently orbiting aboard three Metop (Meteorological Operational) satellites and offer global coverage twice daily with high horizontal resolution (ground pixel diameter at nadir is 12 km). The IASI CH$_4$ products have a particular good quality and sensitivity as documented in validation studies (e.g., Siddans et al., 2017; De Wachter et al., 2017; García et al., 2018; Schneider et al., 2021a).

Here we use the IASI CH$_4$ product as generated by the latest MUSICA IASI processor version (Schneider et al., 2021b). Combining these IASI profile data with the TROPOMI total column data causes strong synergies.
Schneider et al. (2021a) developed an a posteriori method for such a synergistic combination and documented the possibility to detect tropospheric partial column-averaged dry-air molar fractions of CH$_4$ (TXCH$_4$) independently from the upper tropospheric/stratospheric dry-air molar fractions of CH$_4$ (UTSXCH$_4$). This is not possible by either the TROPOMI or IASI product individually. In this study we use a tropospheric product averaged from ground to 7 km a.s.l. and an upper tropospheric/stratospheric product averaged from 7 to 20 km a.s.l.

2.2 COCCON Madrid campaign

Madrid is located on the Meseta Central and 60 km south of the Guadarrama mountains with a considerable altitude difference across the city, ranging from 570 to 700 m a.s.l.

This work was made in the framework of the MEGEI-MAD project (García et al., 2019), which aimed to measure atmospheric concentrations of GHGs in an urban environment combining FTIR instruments and ground-level analyzers. Another objective of MEGEI-MAD was to analyze the possible use of portable COCCON instruments to shape an operational network for Madrid in the future. The MEGEI-MAD project was initiated by the Izaña Atmospheric Research Center (AEMet), in cooperation with two German research groups (the Karlsruhe Institute of Technology and the University of Heidelberg) and two Spanish research groups (the Autonomous University of Barcelona and the University of Valladolid).

Within MEGEI-MAD, a 2-week field campaign was carried out from 24 September to 7 October 2018 in Madrid, where five COCCON instruments were located at five different places circling the metropolitan area (see Fig. 1). Table 1 summarizes the coordinates, altitudes of the COCCON locations and auxiliary meteorological data collected for data analysis of the observations. The locations have been chosen by considering the prevailing winds and the emission sources of CO$_2$ and CH$_4$, as well as other technical and logistic criteria (García et al., 2019, 2021).

2.3 Emission strength calculation using a simple plume model

The daily plume is modeled as a function of wind direction and wind speed. The schematic dispersion model for describing emissions assumes an expanding cone-shaped plume with the tip at the plume source at location (0, 0). The plume cone has an opening angle of size $\alpha$, and any grid cell within the cone is affected by the emission (see Fig. 2). The angle $\alpha$ is a technical parameter to schematically describe a spreading of the plume and is empirically adjusted to a value of 60°. Different opening angles are modeled and presented in Fig. A1. The modeled plume has the most similar shape compared to the TROPOMI measured NO$_2$ plume (see Sect. 3.3) when $\alpha = 60^\circ$. If the grid cell $(x, y)$ locates inside the cone, the column enhancement for this cell can be calculated by

$$\Delta \text{column}(x, y) = \frac{\varepsilon}{v \cdot d(x, y) \cdot \alpha},$$

where $\varepsilon$ is the emission strength at the source point in molec. s$^{-1}$, $v$ is the wind speed in m s$^{-1}$, $d$ is the distance between the downwind point and the source, and $\alpha$ is the opening angle of the plume in rad (here assumed to be 60°).

The distance from a general grid cell $(x, y)$ from the source is

$$d(x, y) = \sqrt{x^2 + y^2}.$$

The enhanced dry-air volume mixing ratio for target species ($\Delta \text{XVMR}$) at the center of the grid cell $(x, y)$ can then be calculated by dividing the column enhancement by the total column of dry air (column$_{\text{dryair}}$):

$$\text{XVMR} = \frac{\Delta \text{column}(x, y)}{\text{column}_{\text{dryair}}}.$$

The column$_{\text{dryair}}$ is computed from the surface pressure:

$$\text{column}_{\text{dryair}} = \frac{P_s}{m_{\text{dryair}} \cdot g(\varphi)} - \frac{m_{\text{H}_2\text{O}}}{m_{\text{dryair}}} \cdot \text{column}_{\text{H}_2\text{O}},$$

where $P_s$ is the surface pressure, $m_{\text{dryair}}$ and $m_{\text{H}_2\text{O}}$ are the molecular masses of dry air ($\sim 28.96$ g mol$^{-1}$) and water vapor ($\sim 18$ g mol$^{-1}$), respectively, column$_{\text{dryair}}$ and column$_{\text{H}_2\text{O}}$ are the total column amount of dry air and water vapor, and $g(\varphi)$ is the latitude-dependent surface acceleration due to gravity.

In this study, each individual landfill is considered an individual point source. The daily plumes from the individual landfills are super-positioned to have a total daily plume. The averaged enhancement of XVMR (plume) over the study area is computed for the selected wind sector. The plume for the opposite wind regime is also constructed in the same manner. The differences between these two data sets are therefore the wind-assigned anomalies (see Sect. 3.3). By fitting the modeled wind-assigned anomalies to the anomalies as observed by the satellite, we can estimate the actual emission strength (see Sect. B2). Note that the applied calculation scheme would also be extendible to areal sources by superimposing such calculations using different locations of the origin.

3 Results and discussion

3.1 Intercomparison of TROPOMI and COCCON XCH$_4$ measurements

To detect whether TROPOMI is capable of measuring XCH$_4$ precisely in the Madrid area, we perform intercomparison between TROPOMI and COCCON XCH$_4$ measurements. Figure 3 shows the correlation between COCCON and
Table 1. Locations of the five COCCON instruments and meteorological records for the MEGEI-MAD field campaign during 24 September–7 October 2018.

| Station         | EM27/SUN | Latitude (° N) | Longitude (° W) | Altitude (m a.s.l.) | Meteorological records                          |
|-----------------|----------|---------------|----------------|---------------------|-----------------------------------------------|
| Tres Olivos     | KIT SN53 | 40.499        | 3.689          | 736                 | Data logger from AEMet Barajas Airport         |
| Barajas         | AEMet SN85 | 40.465     | 3.581          | 637                 | Barajas Airport                               |
| Jose Echegaray  | DLR SN69 | 40.379        | 3.613          | 633                 | Data logger from DLR Cuatro Vientos Airport    |
| Cuatro Vientos  | KIT SN52 | 40.368        | 3.780          | 703                 | Cuatro Vientos Airport                        |
| AEMet           | KIT SN81 | 40.452        | 3.724          | 685                 | AEMet headquarters                             |

Figure 1. Locations of the five COCCON instruments used in the Madrid field campaign during 24 September–7 October 2018, represented with red stars, and locations of three waste treatment and disposal plants, represented with the green triangles (image © Google Earth).

TROPOMI measurements. The mean value of TROPOMI XCH$_4$ is calculated by collecting observations within a radius of 5 km around each COCCON station. The coincident COCCON mean XCH$_4$ is calculated from the measurements within 30 min before or after the TROPOMI overpass. The distance between two stations ranges between 6 and 14.2 km. The TROPOMI data within a circle with a larger radius might cover the information from other nearby stations, which brings an error in the correlation between the coincident data. Therefore, we choose a collection circle with a radius of 5 km for TROPOMI. The coincident data at each station show generally good agreement. Note that there are 1 to 2 TROPOMI measurements located within a circle of 5 km radius around each station. The mean bias in XCH$_4$ between TROPOMI and COCCON is 2.7 ± 13.2 ppb, which is below the absolute bias between TROPOMI and TCCON (3.4 ± 5.6 ppb, Lorente et al., 2021a). The higher scatter of the validation with COCCON reflects the shorter temporal and spatial collocation, but the agreement indicates that TROPOMI data have good quality and a low bias.

The coincident data on 25 September 2018 and 4 October 2018 show large biases at Jose Echegaray station where the SN69 COCCON instrument is located. Due to its coarser spatial resolution, the TROPOMI XCH$_4$ observations do not capture the local enhancements detected by the COCCON instrument in the vicinity of the source. Figure 4 illustrates the 2 example days of the time series of COCCON SN69 and coincident TROPOMI observations. Obvious enhancements are observed at around 13:00 UTC by the COCCON instrument in the downwind site on 25 September and at around 12:30 on 4 October 2018 (see Fig. A2 for the other days). Note that the XCH$_4$ enhancements can also be observed by the instruments at other stations when the CH$_4$ plume passes over Madrid. We only discuss the 2 representative days with obvious enhancements here, as we focus on the specific source near the Jose Echegaray station. The Valdemingómez and Pinto waste
value fits well with the wind velocity observed at the Cuatro Vientos Airport.

TROPOMI detected 10 ppb higher $X_{CH_4}$ at Jose Echegaray station than at Barajas station on 25 September 2018. However, COCCON observed a much higher amount of $X_{CH_4}$ (53 ppb) at Jose Echegaray station than at Barajas station (and other stations) at around 13:00 UTC. The delayed enhancements at AEMet and Barajas stations at the downwind direction are found after the wind direction changed from north more towards south direction. Another obvious enhancement of $X_{CH_4}$ is observed at Jose Echegaray station by the COCCON SN69 instrument at around 12:30 on 4 October 2018, with about 97 ppb higher $X_{CH_4}$ than COCCON measurements at the other four stations. However, TROPOMI only measured about 13 ppb higher $X_{CH_4}$ at Jose Echegaray station compared to the TROPOMI measurements at the other stations. These considerable enhancements at Jose Echegaray station observed by the COCCON instrument are likely due to the local source (the nearby Valdemingómez waste plant). The plume is in close vicinity to the source narrower than the pixel scale of the satellite, and therefore it is only detected as an attenuated signal by TROPOMI. The full width at the half maximum (FWHM) of the enhancement peak on 4 October 2018 roughly covers a temporal window of 30 min, with a corresponding wind direction change of 22.5° (~0.4 rad) and an averaged wind speed of 1.0 m s$^{-1}$. The distance between the COCCON SN69 to the Valdemingómez waste plant is about 4500 m. The 97 ppb enhancement measured by COCCON SN69 instrument yields an estimated emission strength of $3.7 \times 10^{25}$ molec. s$^{-1}$.

According to the Spanish Register of Emissions and Pollutant Sources (PRTR, http://www.en.prtr-es.es/, last access: 20 February 2021), more than 95% of total $CH_4$ emissions are from three waste treatment and disposal plants in the Madrid region (locations showed in Fig. 1). The annual $CH_4$ emission rates from the PRTR for each plant are listed in Table 2. The total emission strength for each plant is about $2.5 \times 10^{25}$ molec. s$^{-1}$. This value only considers the "cells" in production, i.e., those where the waste is not yet covered with soil. The emissions from sealed cells are not included in the total emissions, but they still emit $CH_4$ for years after sealing. So, the estimated emission rates from the inventories are expected to underestimate the true emissions, which fits reasonably with the estimated emission rate derived from COCCON measurements. The COCCON instruments show a very good ability to detect the source. Based on this evidence we investigate the potential of the TROPOMI and IASI $CH_4$ products for detecting $CH_4$ sources in the following.

3.2 Predominant wind

To better represent the whole area of Madrid, the hourly ERA5 model wind at a height of 10 m around Madrid is used. ERA5 is the fifth-generation climate reanalysis pro-
Figure 4. Time series of COCCON measurements at five stations on 2 d in 2018. Star symbols represent the averaged TROPOMI observations within a radius of 5 km around each station. Lower panels show the wind direction and wind speed measured at the Cuatro Vientos Airport.

Table 2. CH\textsubscript{4} emission rates in three waste treatment and disposal plants in Madrid from PRTR.

| Waste treatment and disposal plants | Valdemingómez (molec. s\textsuperscript{-1}) | Pinto (molec. s\textsuperscript{-1}) | Alcalá (molec. s\textsuperscript{-1}) | Total (molec. s\textsuperscript{-1}) |
|------------------------------------|---------------------------------------------|-------------------------------------|------------------------------------|-------------------------------------|
| 2017                               | \(7.4 \times 10^{24}\)                      | \(1.2 \times 10^{25}\)              | \(2.1 \times 10^{24}\)              | \(2.2 \times 10^{25}\)              |
| 2018                               | \(7.4 \times 10^{24}\)                      | \(1.3 \times 10^{25}\)              | \(2.1 \times 10^{24}\)              | \(2.2 \times 10^{25}\)              |
| 2019                               | \(9.8 \times 10^{24}\)                      | \(1.4 \times 10^{25}\)              | \(9.4 \times 10^{23}\)              | \(2.5 \times 10^{25}\)              |

produced by the European Centre for Medium-Range Weather Forecasts (ECMWF) (Copernicus Climate Change Service, 2017). The TROPOMI overpasses over Madrid cover the time range from 12:00–14:30 UTC (IASI overpasses are typically from 09:30–10:30 UTC), but the dispersion of emitted CH\textsubscript{4} is influenced by the ground conditions (e.g., wind speed and wind direction) over a wider time range (Delkash et al., 2016; Rachor et al., 2013). Therefore, the wind information between daytime (08:00–18:00 UTC) is chosen to define the predominant wind direction for each day. Figure 5 presents the wind roses for daytime between 10 November 2017 and 10 October 2020 (the first and last day with valid TROPOMI data). The dominating wind direction was south-westerly. The Guadarrama mountains and the Jarama and Manzanares river basins are located the northwest of Madrid, and they influence the air flow. Therefore, we use a wider wind range for the specific wind area in this study to cover the dominant wind directions, i.e., SW for the range of 135–315° and NE for the remaining direction. If a wind direction dominates 60% of records for 1 d, i.e., if the wind direction belongs to one specific area more than 60% of the daytime (08:00–19:00 UTC), then this predominant wind direction is selected for that day. The SW and NE wind fields are used for constructing wind-assigned anomalies in this study, and we demonstrate this construction by using TROPOMI nitrogen dioxide (NO\textsubscript{2}) data in the next section. Table 3 summarizes the number of days and wind speed for each specific wind area. The wind direction during the TROPOMI overpasses was 61.8% in the SW wind field and 28.4% in the NE wind field, and their averaged wind speed is similar.

3.3 Demonstration of the wind-assigned anomaly method

When fossil fuels are burned, nitrogen monoxide (NO) is formed and emitted into the atmosphere. NO reacts with O\textsubscript{2} to form NO\textsubscript{2} and with ozone (O\textsubscript{3}) to produce O\textsubscript{2} and NO\textsubscript{2}. NO\textsubscript{2} is an extremely reactive gas with a short lifetime of a couple of hours and has lower background levels than CH\textsubscript{4} (Kenagy et al., 2018; Shah et al., 2020). It is measured by TROPOMI with excellent quality. Therefore, it is a suitable proxy for demonstrating the method developed for the wind-assigned anomaly.

TROPOMI offers simultaneous observations of NO\textsubscript{2} columns. The recommended quality filter value for the analysis of TROPOMI NO\textsubscript{2} columns is qa_value > 0.75 (http://www.tropomi.eu/sites/default/files/files/publicSentinel-SP-Level-2-Product-User-Manual-Nitrogen-Dioxide.pdf,
Figure 5. Wind roses for daytime (08:00–19:00 UTC) from 10 November 2017 to 10 October 2020 for the ERA5 model wind. Panel (a) covers all days and panel (b) covers the days with TROPOMI overpasses.

Table 3. Number of days and the averaged ERA5 wind speed (± standard deviation) per specific wind area in daytime (08:00–18:00 UTC) from 10 November 2017 to 10 October 2020. Columns 2 and 3 are for all days, and columns 4 and 5 are for days with TROPOMI overpass.

| Wind direction range | Number of days in total (%) | Averaged wind speed ± standard deviation (m s\(^{-1}\)) | TROPOMI overpass | Number of days in total (%) | Averaged wind speed ± standard deviation (m s\(^{-1}\)) |
|----------------------|-----------------------------|--------------------------------------------------------|------------------|-----------------------------|--------------------------------------------------------|
| NE/＞315° or ＜135°   | 30.4                        | 2.6 ± 1.5                                              | 28.4             | 2.3 ± 1.2                   |
| SW/135–315°          | 68.4                        | 2.8 ± 1.7                                              | 61.8             | 2.3 ± 1.4                   |

Based on the predominant wind direction in Madrid (see Sect. 3.2), the averaged wind-assigned anomalies are defined here as the difference of the mean TROPOMI NO\(_2\) column under the wind direction from NE and the mean TROPOMI NO\(_2\) column under the predominant wind direction of SW in Madrid.

Figure 6a illustrates the wind-assigned anomalies of TROPOMI NO\(_2\) (ΔNO\(_2\)) on a 0.1° × 0.135° latitude-longitude grid during 2018–2019. Pronounced fusiform-shaped plumes are observed along NE–SW wind direction as expected. Figure 6b shows the wind-assigned anomalies derived from the simple model introduced in Sect. 2.3, using Madrid city center as the point source with an assumed emission rate (ε) of 5.0 × 10\(^{24}\) molec. s\(^{-1}\) and using ERA5 10 m wind data. The similar symmetrical positive and negative plumes to those in Fig. 6a imply that our method of wind-assigned anomaly is working as anticipated, that the ERA5 10 m data are indeed representative for the area and that the implementation of the satellite data analysis is correct. Figure 6c shows the strong correlation between the wind-assigned anomalies derived from the TROPOMI measurements and the simple plume model (ε = 5.0 × 10\(^{24}\) molec. s\(^{-1}\)). Using the fitting method as described in Sect. B2, we estimate an emission rate of 3.5 × 10\(^{24}\) molec. s\(^{-1}\) ± 3.9 × 10\(^{22}\) molec. s\(^{-1}\). Here the uncertainty is due to the noise of the observations and is calculated according to Eq. (B15) (Appendix B). This estimated source strength is weaker than the strength obtained by Beirle et al. (2011), where the reported NO\(_x\) emission is around 150 mol s\(^{-1}\) in Madrid, corresponding to a NO\(_2\) emission of 6.8 × 10\(^{25}\) molec. s\(^{-1}\). It is because our model does not consider the decay of NO\(_2\), which results in a lower emission rate.

The result of this test using NO\(_2\) also allows the angular spread parameter used in the plume model to be adjusted (see Sect. 2.3 and Eq. 3). As it can be seen from Fig. A1, assuming an angular spread of 60° reasonably reproduces the shape of the plume.

3.4 XCH\(_4\) and TXCH\(_4\) anomaly

CH\(_4\) has a relatively longer lifetime as compared to NO\(_2\), and its background in the atmosphere is high. An increasing
trend with obvious seasonality and strong day-to-day signals for XCH$_4$ is seen in Fig. 7 (upper panels). Therefore, these background signals need to be removed before simulating the wind-assigned anomalies (see Sect. B1). After removing the background, the anomalies (raw data – background) represent more or less the emission from local area (Fig. 7 lower panels).

Figure 8 illustrates the anomalies of XCH$_4$, TXCH$_4$ and UTSXCH$_4$ for all measurement days, days with predominating SW wind field and days with predominating NE wind field. The distributions over the whole area for XCH$_4$ and TXCH$_4$ are similar, and no obvious enhancement is observed in UTSXCH$_4$, as expected, since CH$_4$ abundances dominate in the troposphere. The areas where the three waste plants are located show obvious high anomalies in the figures (Fig. 8a and d) when the data are averaged over all days for all wind directions and in the downwind direction (Fig. 8b, c, e and f), demonstrating that our method of removing the background works well and the satellite products can detect the local pollution sources after removing the background. Enhanced plumes of XCH$_4$ and TXCH$_4$ are better visible on the downwind side of SW than on the downwind side of NE wind field. This is because the SW is the most dominant wind direction, and the SW plume signal is based on a higher number of data and thus less noise.

3.5 Estimation of CH$_4$ emission strengths from satellite data sets

The wind-assigned anomalies derived from XCH$_4$ anomalies and TXCH$_4$ anomalies on a $0.1^\circ \times 0.135^\circ$ latitude–longitude grid are presented in Fig. 9. The XCH$_4$ and TXCH$_4$ wind-assigned anomalies show similar bipolar plumes but are more disturbed compared to those derived from NO$_2$. This is because the CH$_4$ signal is weak compared to the background concentration, so the noise level of the measurement and the imperfect elimination of the background are significant disturbing factors.

Based on the knowledge of the locations of the three waste plants, we choose their locations as point sources to model the enhanced XCH$_4$ according to the wind information. The initial emission strength is $1 \times 10^{26}$ molec. s$^{-1}$ in total, and the emission rate at each point source is repartitioned among these three sites according to Table 2. The modeled and observed wind-assigned anomalies show a reasonable linear correlation (coefficient of determination $R^2$ of about 49% and 44% for XCH$_4$ and TXCH$_4$, respectively) with observed ΔXCH$_4$. Based on Eq. (B12) (Appendix B), we obtained an estimated emission rate of $7.4 \times 10^{25} \pm 6.4 \times 10^{24}$ molec. s$^{-1}$ for XCH$_4$ and $7.1 \times 10^{25} \pm 1.0 \times 10^{25}$ molec. s$^{-1}$ for TXCH$_4$. The uncertainty values given here are the square root sum of the uncertainty due to the background signal and the data noise, which are calculated according to Eqs. (B14) and (B15) (Appendix B). Figure 9g, h and i show the wind-assigned anomalies for UTSXCH$_4$. For the modeled UTSXCH$_4$ anomalies we assume here the CH$_4$ enhancement to occur at altitudes between 7 and 20 km a.s.l. As expected, the fit of these model data to the observed UTSXCH$_4$ data yields emission rates close to zero ($1.4 \times 10^{25} \pm 7.2 \times 10^{24}$ molec. s$^{-1}$), revealing that there is no significant plume signal above 7 km a.s.l. The fact that for TXCH$_4$ we obtain practically the same emission rates as for XCH$_4$ and that in the UTSXCH$_4$ data we see almost no plume nicely proves the quality of our careful background treatment method and the low level of cross sensitivity between the TXCH$_4$ and UTSXCH$_4$ data products. The applied background treatment allows detecting the
Figure 7. Time series of (a) XCH$_4$, (b) TXCH$_4$ and (c) UTXSCH$_4$, showing raw data and background in each upper panel and anomalies in each corresponding lower panel.

near-surface emission signal consistently in the total column XCH$_4$ data and in the tropospheric TXCH$_4$ data.

Figure 10 illustrates the estimated emission strengths for the different products. The emission strengths derived from the satellites are higher than the ones derived from COCCON measurements, as TROPOMI covers a larger area, while COCCON measurements are only sensitive to local sources from the nearby waste plant. The PRTR inventory document gives lower values than our results. This is probably because it only lists the active landfill cells and does not include the closed ones in Madrid, which probably still emit for many years (Sánchez et al., 2019).

3.6 Sensitivity study for emission strength estimates

The point sources and their proportion in the total emission rate in this study are based on the a priori knowledge of three different waste plant locations. If we use a single source located at the Pinto waste disposal site only, it yields an emis-
Figure 8. (a–c) $XCH_4$, (d–f) $TXCH_4$ and (g–i) $UTSXCH_4$ anomalies averaged for all days, days with SW wind and NE wind directions. The triangle symbols represent the location of waste plants.
Figure 9. Wind-assigned XCH₄ plume derived from (a) TROPOMI XCH₄ anomalies, (d) synergetic TXCH₄ anomalies, and (g) UTSXCH₄ anomalies and their corresponding modeled plume (b, e, h) over Madrid in the NE–SW direction on a 0.1° × 0.135° latitude–longitude grid. The correlation plots between observed ΔXCH₄ and modeled ΔXCH₄ ($\epsilon = 1 \times 10^{26}$ molec. s$^{-1}$) for different products (c, f, i). Here we use the three waste plants as the point sources (blue triangle with red edge color). The initial emission rate in the plume model is $1 \times 10^{26}$ molec. s$^{-1}$. This value is proportionally distributed into three point sources based on the a priori knowledge of emission rate in each waste plant. For the modeled UTSXCH₄ anomalies we assume the CH₄ enhancements to occur at altitudes between 7 and 20 km a.s.l.
sion rate of 6.3 × 10^{25} \text{ molec. s}^{-1}, \sim 15\% lower than that of the three point sources for CH\textsubscript{4} and 6.0 × 10^{25} \text{ molec. s}^{-1} (−15\%) for tropospheric CH\textsubscript{4} (see Fig. 10). The opening angle (\(\alpha\)) is experimentally selected based on the comparison between the TROPOMI measured and modeled NO\textsubscript{2} plume, which results in some uncertainties as well. Using 90\° instead of 60\° for \(\alpha\) in the plume model results in an emission strength of 7.6 × 10^{25} \text{ molec. s}^{-1} (+3\% change) for CH\textsubscript{4} and of 7.4 × 10^{25} \text{ molec. s}^{-1} (+4\% change) for tropospheric CH\textsubscript{4}.

The surface wind can be influenced by the topography, and the actual transport pathway from the emission source to the measurement station is difficult to know (Chen et al., 2016; Babenhausreheide et al., 2020). To study the wind sensitivity, the hourly wind information measured at the Cuatro Vientos Airport at 10 m height is used instead of the ERA5 10 m wind. There are other in situ measurements available but not used here, as the AEMet headquarter station is affected by nearby buildings and the Barajas Airport station is very close to a river (Jarama) that determines a specific wind pattern. The wind measured at the Cuatro Vientos Airport is quite different compared to the ERA5 wind, as in situ-measured NE wind becomes dominant as well, and the wind speed in SW wind field increases by \sim 50\% compared to that of ERA5 wind (Figs. A3, A4 and Table A1). Using the wind measured at the Cuatro Vientos Airport results in an emission rate of 7.7 × 10^{25} \text{ molec. s}^{-1} (+4\%) for CH\textsubscript{4} and 9.5 × 10^{25} \text{ molec. s}^{-1} (+34\%) for tropospheric CH\textsubscript{4}.

In summary, the uncertainties derived from the source location, opening angle or wind cannot be ignored, but nevertheless the emission rates estimated from the spaceborne observations are clearly larger than the values reported in Table 2 and are larger than the ones estimated from the COCCON SN69 observations in October 2018.

4 Conclusions

The present study analyzes TROPOMI XCH\textsubscript{4} and IASI CH\textsubscript{4} retrievals over an area around Madrid for more than 400 d within a rectangle of 39.5–41.5\° N and 4.5–3.0\° W (125 km × 220 km) from 10 November 2017 until 10 October 2020. During this time period, a 2-week field campaign was conducted in September 2018 in Madrid, in which five ground-based COCCON instruments were used to measure XCH\textsubscript{4} at different locations around the city center.

First, TROPOMI XCH\textsubscript{4} is compared with co-located COCCON data from the field campaign, showing a generally good agreement, even though the radius of the collection circle for the satellite measurements was as small as 5 km. However, there are 6 d when obvious enhancements due to local sources were observed by COCCON around noon at the most southeast station (Jose Echegaray), which were underestimated by TROPOMI. The ground-based COCCON observations indicate a local source strength of 3.7 × 10^{25} \text{ molec. s}^{-1} from observations at Jose Echegaray station on 4 October 2018, which is reasonable compared to the emissions assumed for nearby waste plants. The waste plant locations are later used as the point sources to model the emission strength for CH\textsubscript{4}.

According to the ERA5 model wind at 10 m height, SW (135–315\°) winds (NE covering the remaining wind field) are dominant in the Madrid city center in the time range from November 2017 to October 2020. Based on this wind information, the wind-assigned anomalies are defined as the difference of satellite data between the conditions of the NE wind field and SW wind field. We use the simultaneously measured tropospheric NO\textsubscript{2} column amounts from TROPOMI as a proxy to evaluate the wind-assigned anomaly approach due to its short lifetime and clear plume shape, by using ERA5 model wind. Pronounced and bipolar NO\textsubscript{2} plumes are observed along the NE–SW wind direction, and a tropospheric NO\textsubscript{2} emission strength of 3.5 × 10^{24} ± 3.9 × 10^{22} \text{ molec. s}^{-1} is estimated. This implies that our method of wind-assigned anomaly is working reliably, that the ERA5 wind data used are indeed representative of the area and the implementation of the satellite data analysis is correct.

CH\textsubscript{4} is a long-lived gas and so there are strong CH\textsubscript{4} background signals in the atmosphere. Therefore, the background values need to be removed and the anomalies have to be determined before calculating emission strengths. In this study, the removed background values include the linear increase, seasonal cycle, daily variability and horizontal variability. The areas where the three waste plants are located show obvious high anomalies, demonstrating that satellite measurements can detect the local sources after removing the back-
Enhanced plumes are more pronounced in the downwind side of SW, whereas the observed downwind plume signal for NE wind is noisier, partly due to the lower number of NE wind situations.

The wind-assigned TROPOMI XCH$_4$ anomalies show a less clear bipolar plume than NO$_2$. This is because CH$_4$ has a long lifetime, and its high background is difficult to totally remove. Based on the wind-assigned anomalies, the emission strength estimated from the TROPOMI XCH$_4$ data is $7.4 \times 10^{25} \pm 6.4 \times 10^{24}$ molec. s$^{-1}$. In addition, this method is applied to the tropospheric partial column-averaged (ground – 7 km a.s.l.) dry-air molar fractions of methane (TXCH$_4$, obtained by combining TROPOMI and IASI products), yielding an emission strength of $7.1 \times 10^{25} \pm 1.0 \times 10^{25}$ molec. s$^{-1}$. We show that in the upper troposphere/stratosphere there is no significant plume signal ($1.4 \times 10^{25} \pm 7.2 \times 10^{24}$ molec. s$^{-1}$). The estimation of very similar emission rates from XCH$_4$ and TXCH$_4$ together with the estimated negligible emission rates when using data representing the upper troposphere/stratosphere proves the robustness of our method. The emission rates derived from satellites (XCH$_4$ and TXCH$_4$) are higher than that derived from COCCON observations, as satellites cover larger areas with other CH$_4$ sources and COCCON likely measures local sources.

The surface wind is easily influenced by the topography, which introduces uncertainties in the estimated emission strengths. Using in situ-measured wind at the Cuatro Vientos Airport instead of ERA5 model wind results in an estimated emission rate of $7.7 \times 10^{25}$ molec. s$^{-1}$ (+4%) for CH$_4$ and $9.5 \times 10^{25}$ molec. s$^{-1}$ (+34%) for tropospheric CH$_4$. Uncertainties can also be caused by the choice of the opening angle in the plume model. The estimated emission rates with $\alpha = 90^\circ$ are $7.6 \times 10^{25}$ molec. s$^{-1}$ (+3%) for CH$_4$ and $7.4 \times 10^{25}$ molec. s$^{-1}$ (+4%) for tropospheric CH$_4$. When using a single source located in the Madrid city center, the emission strengths are $6.3 \times 10^{25}$ molec. s$^{-1}$ ($-15\%$) for CH$_4$ and $6.0 \times 10^{25}$ molec. s$^{-1}$ ($-15\%$) for tropospheric CH$_4$.

In summary, in this study for the first time TROPOMI observations are used together with IASI observations and the ground-based COCCON observations to investigate CH$_4$ emissions from landfills in an important metropolitan area like Madrid. The COCCON instruments show a promising potential for satellite validation and an excellent ability for observation of local sources. The data presented here show that TROPOMI is able to detect the tropospheric NO$_2$ and CH$_4$ anomalies over metropolitan areas with support from meteorological wind analysis data. This methodology could also be applied to other source regions, space-based sensors and sources of CO$_2$. 
Appendix A

**Table A1.** Number of days and the averaged wind speed (±standard deviation) per specific wind area in daytime (08:00–18:00 UTC) from 10 November 2017 to 11 September 2020 measured at the Cuatro Vientos Airport. Columns 2 and 3 are for all days, and columns 4 and 5 are for days with TROPOMI overpass.

| Wind direction range | Number of days in total (%) | Averaged wind speed ± standard deviation (m s<sup>-1</sup>) | Number of days in total (%) | Averaged wind speed ± standard deviation (m s<sup>-1</sup>) |
|----------------------|-----------------------------|-----------------------------------------------------------|-----------------------------|-----------------------------------------------------------|
| NE/>315° or <135°    | 35.4                        | 2.4 ± 1.5                                                 | 36.0                        | 2.2 ± 1.3                                                 |
| SW/135–315°          | 49.3                        | 4.2 ± 2.5                                                 | 44.4                        | 3.4 ± 2.1                                                 |

**Figure A1.** Examples of wind-assigned NO<sub>2</sub> plume based on the simple plume model ($\varepsilon = 5.0 \times 10^{24}$ molec. s<sup>-1</sup>) using Madrid as the point source in the NE–SW direction on a 0.1° × 0.135° latitude–longitude grid with a different opening angle ($\alpha$) from 10 to 90°.

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Figure A2. Time series of COCCON measurements at five stations and corresponding time series of wind fields (direction and speed) measured at the Cuatro Vientos Airport on 8 d during MEGE1-MAD campaign in 2018. Star symbols represent the TROPOMI observations within a radius of 5 km around each station.
Figure A3. Percentage of occurrence for wind direction measured at the Cuatro Vientos Airport between 2000 and 2020. The predominant wind direction is southwest and up to 35% of time.

Figure A4. Wind roses for daytime (08:00–19:00 UTC) from 10 November 2017 to 11 September 2020 from the wind measurements at the Cuatro Vientos Airport. Panel (a) covers all days and panel (b) covers the days with TROPOMI overpasses.
Appendix B

B1 CH₄ background signal

The satellite data can be written as a vector \( y \), where each element corresponds to an individual satellite data point. This signal is caused by a CH₄ background signal and the CH₄ plume due to the emissions from the waste disposal sites near Madrid:

\[
y = y_{BG} + y_{plume}.
\]  

(B1)

It is of great importance to adequately separate both components for estimating the emission strength from the satellite data.

For determining the background signal \((y_{BG})\), we set up a background model:

\[
m_{BG} = y_{BG} = K_{BG}x_{BG}.
\]  

(B2)

The matrix \( K_{BG} \) is a Jacobian matrix that allows us to reconstruct the background according to a few background model coefficients (the elements of the vector \( x_{BG} \)). We also create a Jacobian \( K_{BG}^{*} \), which is the same as \( K_{BG} \) but set to zero for observations where the wind data suggest a significant impact of the CH₄ plume on the satellite data. The calculations of the plume CH₄ signals are made according to Sect. 2.3. With the use of \( K_{BG}^{*} \), we make sure that the estimated background signal is not affected by the CH₄ plume.

The \( K_{BG} \) is a Jacobian matrix where each row represents an individual satellite observation and each column represents a component of the background model. The background model considers a smooth background, which is a constant CH₄ value, a linear increase with time, and a seasonal cycle described by the amplitude and phase of the three frequencies 1/year, 2/year and 3/year. Furthermore, we fit a daily anomaly, which is the same for all data measured during a single day, and a horizontal anomaly, which is the same for any time but dependent on the horizontal location. For the latter we use a \( 0.1^\circ \times 0.135^\circ \) (latitude × longitude) grid.

We invert the problem in order to estimate the background model coefficients (elements of the vector \( x_{BG} \)):

\[
\hat{x}_{BG} = G_{BG}y,
\]  

(B3)

with \( G_{BG} \) being the so-called gain matrix,

\[
G_{BG} = (K_{BG}^{*})^T S_{y,n}^{-1} K_{BG}^{*} + S_{a}^{-1} - 1 K_{BG}^{*} S_{y,n}^{-1}.
\]  

(B4)

Because \( K_{BG}^{*} \) (and thus \( G_{BG} \)) is set to zero whenever \( y_{plume} = 0 \), we can use in Eq. (B3) \( y \) instead of \( y_{BG} \). The matrix \( S_{y,n} \) stands for the noise covariance of the satellite data. For constraining the problem, we use a diagonal \( S_{a}^{-1} \) (no constraint between different coefficients) with a very low constraint value for the coefficient determining the constant and higher constraint values for the other coefficients. For calculating the uncertainty of the background signal, we calculate the vector \( y - K_{BG}^{*} \hat{x}_{BG} \) and then the mean square value from its elements that represent observations not affected by the plume. This mean square value is then used as the diagonal entries of the diagonal matrix \( S_{y,BG} \). In this context, \( S_{y,BG} \) considers the deficits of the background model and the uncertainty in the background if determined from data with a certain noise level. As an alternative, we could use modeled high-resolution XCH₄ fields (e.g., from CAMS high-resolution greenhouse gas forecast, Barré et al., 2021) for these calculations. We can assume that the model data have no noise and perform an exclusive estimation of the deficits of the background model calculation in form of a full \( S_{y,BG} \) covariance matrix. This more sophisticated uncertainty estimation can be a task for future work.

The uncertainty of the background model coefficients can be calculated as

\[
S_{\hat{x}_{BG}} = G_{BG} S_{y,BG} G_{BG}^T.
\]  

(B5)

For each day there is an uncertainty in the background coefficients and the uncertainty is correlated with the uncertainty at other days. All this information is provided in the uncertainty covariance \( S_{y,BG} \).

With the full Jacobian \( K_{BG} \) we can now model the background for the measurement state (also for the measurements that are assumed to be affected by the CH₄ waste disposal plume),

\[
y_{BG} = K_{BG} \hat{x}_{BG}.
\]  

(B6)

and calculate the plume signal according to Eq. (B1) as

\[
y_{plume} = y - K_{BG} \hat{x}_{BG}.
\]  

(B7)

The uncertainty of these plume signal is the sum of the uncertainties of the satellite data \( S_{y,n} \) and the uncertainty of the estimated background:

\[
S_{y,plume} \approx S_{y,n} + K_{BG} S_{BG} K_{BG}^T.
\]  

(B8)

It notes that Eq. (B8) is an approximation, because the two error components are not completely independent \( (S_{BG} \) and thus \( S_{\hat{x}_{BG}} \) depend also on the noise of the observations; see description for calculating \( S_{y,BG} \) in the context of Eq. B5).

B2 Fitting of CH₄ emission rates

Because the CH₄ plume signal is rather weak compared to the CH₄ background uncertainty and the noise level of the satellite data, we have to work with averages in order to reduce the data noise. The averaging is made by classifying the observation in two predominant wind categories. We calculate the average plume maps for the southwest and northeast wind situations (see Figs. 6 and 8). Then we calculate the difference between the southwest and northeast plume maps (the wind-assigned anomalies or \( \Delta \)-maps). All the calculations are made by binning all observations that fall within a certain \( 0.135^\circ \times 0.1^\circ \) (longitude × latitude) area. In order to
significantly reduce the data noise, we only consider averages for the \(0.135^\circ \times 0.1^\circ\) areas based on at least 25 individual observations made under southwest wind conditions and 25 individual observations made under northeast wind conditions. The binning, the averaging, the wind-assigned \( \Delta \)-maps calculations and the data number filtering are achieved by operator \( D \), and we can write

\[
\Delta y_{\text{plume}} = Dy_{\text{plume}}
\]

and

\[
\Delta S_{y, \text{plume}} = DS_{y, \text{plume}}D^T.
\]

Here \( \Delta y_{\text{plume}} \) is a column vector whose elements capture the different signal of the two wind directions at the different locations, and \( \Delta S_{y, \text{plume}} \) is the corresponding uncertainty covariance.

For modeling the plume signals we use a priori knowledge of \( \text{CH}_4 \) emission locations, i.e., assuming a repartition of the emissions between the three waste disposal sites according to Table 2 (see Sect. 3.1). Together with information from the wind, we then model the \( \text{CH}_4 \) plume’s wind-assigned anomaly signal \( \Delta y_{\text{plume}} \):

\[
\Delta y_{\text{plume}} = \Delta k x.
\]

Here the Jacobian \( \Delta k \) (a column vector) represents the wind-assigned anomaly model as described in Sect. 2.3. It describes how an emission at the waste disposal sites according to Table 2 would be seen in the difference signal. We are interested in the coefficient \( x \) (a scalar describing how the assumed emissions from Table 2 have to be scaled by a common factor in order to achieve the best agreement with the observed plume).

Similar to Eqs. (B3) and (B4) we write

\[
\hat{x} = g^T \Delta y_{\text{plume}},
\]

with the row vector

\[
g^T = (\Delta k^T \Delta S_{y, \text{plume}}^{-1} \Delta k)^{-1} \Delta k^T \Delta S_{y, \text{plume}}^{-1}.
\]

This fitting of the emission rate correctly considers the respective uncertainty of the difference signals at the different locations.

Because of the small plume signals, it is important to estimate the reliability of the fitted emission rate. The uncertainty of \( x \) due to the background uncertainty and the noise in the satellite data can be estimated as

\[
\epsilon_{\text{BG}} = \sqrt{g^T D_{\text{BG}} S_{\text{BG}}^{-1} D_{\text{BG}}^T g}
\]

and

\[
\epsilon_n = \sqrt{g^T D_{y,n} D^T g}
\]

respectively. However, as aforementioned these two error components are not completely independent.

Data availability. The data are accessible by contacting the corresponding author (qiansi.tu@kit.edu). The SRON SSP-RemoTeC scientific TROPOMI CH4 data set from this study is available for download at https://doi.org/10.5281/zenodo.4447228 (Lorente et al., 2021b). The MUSICA IASI data set is available for download via https://doi.org/10.35097/408 (Schneider et al., 2021c).

Author contributions. QT, FH and OG developed the research question. QT wrote the manuscript and performed the data analysis with input from FH, OG, MS and FK. FH suggested the method of constructing wind-assigned anomalies for source quantification. MS suggested the method for calculating the anomalies, for fitting the emission rates and for estimating the uncertainty. OG provided the COCCCON and meteorological data and helped to interpret them. TB and AL provided technical support for the TROPOMI data analysis. MS, BE and CJD provided the combined (MUSICA IASI + TROPOMI) data and provided technical support for the analysis of these data. All other coauthors participated in the field campaign and provided the data. All authors discussed the results and contributed to the final paper.

Competing interests. The contact author has declared that neither they nor their co-authors have any competing interests.

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