Three Jahn-Teller states of matter in spin-crossover system Mn(taa)

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The three high-spin phases recently discovered in spin-crossover system Mn(taa) are identified as a low-temperature Jahn-Teller ordered (solid) phase, an intermediate-temperature dynamically correlated (liquid) phase, and an uncorrelated (gas) phase through analysis by first-principles calculation and Monte Carlo simulation. In particular, the Jahn-Teller liquid phase arises from competition between mixing with low-spin impurities, which drives the disorder, and inter-molecular strain interaction. The latter is a key factor in both the spin-crossover phase transition and the magnetoelectric coupling. Jahn-Teller liquids may exist in other spin-crossover materials and materials that have multiple equivalent Jahn-Teller axes.

Jahn Teller (JT) distortions play important roles in many spin-crossovers (SCO) (also known as spin state transitions) in molecule-based magnets [1, 5]. In SCO, the electrons in partially filled d shells transition between orbitals to change the overall spin state. The change of spin state can create or remove JT distortions. Long-range ordering of the JT distortions in the S = 2 HS state of crystalline [Mn3+(pyrl)3(tren)] (Mn(taa)) has been shown [6] to lead to magnetoelectric coupling, which is the interplay between magnetism and electric polarization or dielectric properties. Magnetoelectric coupling offers potential for applications in low-power magnetic sensors, frequency devices, data storage and other applications for moving beyond Moore’s law [7–9]. Molecule-based magnetic materials have recently stimulated much interest because of the global initiative in quantum information science and spintronics. [10, 11] and their low Young’s modulus offers great potential for lattice-mediated magnetoelectric coupling.

In conventional solids such as inorganic perovskites, cooperative JT effects are linked to structural and metal-insulator phase transitions [12, 13], and are crucial in explaining many physical properties of materials such as colossal magneto-resistance [14]. In the molecular solid Mn(taa), JT distortions are also expected to show long-range correlation due to the inter-molecular JT distortion. In the high spin (HS) state, there are three nearly-degenerate JT distortions along axes 120° apart, which reduce the Mn site symmetry from C3 to C1, and also carry electric dipoles. In Ref. [8], a modified four-state Ising-Potts model [15, 16] based on a mean-field approach [17, 18] was used to explain the magnetoelectric behavior in terms of ordering of the three JT distortions and their associated electric dipoles. However, it did not offer a microscopic model for the inter-molecular interactions, nor an exact long-range ordering pattern of JT distortions. Rather, it described the emergence of three HS phases in terms of the statistical distributions of three degenerate JT distortion axes.

In this Letter, we apply first-principles calculations and Monte-Carlo simulations to study the microscopic process underlying the phase transition and magnetoelectric coupling of Mn(taa), explicitly including the inter-molecular correlation of the JT distortion. Through analysis of the correlation function and polarization fluctuation, we show that the three HS phases discovered experimentally correspond to a solid-like phase, where the JT distortions are ordered and uniform, a liquid-like phase, where the JT distortions are disordered with long range correlation, and a gas-like phase, where the JT distortions are uncorrelated. In particular, the JT liquid phase is driven by a competition between disorder, which is caused in part by dynamic mixing with low spin (LS) impurities, and inter-molecular correlation, which is caused by elastic strain. Such a competition also leads to a nonzero macroscopic electric polarization, providing a mechanism for magnetoelectric coupling.

We study a microscopic model on a lattice in which each site represents one Mn(taa) molecule. The Mn3+ cation as the center atom has two possible spin-states: LS with S = 1 and HS with S = 2. The state of each site i is labeled by (s, m, q, {nkl}), where s = ℓ, h denotes the LS (S = 1) and HS (S = 2) state, and m ∈ [−s, s] is the magnetic quantum number. q = 0 for LS and q = x, y, z for HS represent the elongation axis of the JT distortion, and {nkl} is a set of vibration numbers of the on-site phonon mode k of Mn(taa). The indices (s, m, q) denote the spin-JT states, with a total of eighteen states: three LS Sz = 1, 0, −1 and fifteen HS (Sz = 2, 1, 0, −1, −2 and three JT elongation axes), for each site. Therefore, the total Hamiltonian H is written in three parts: the on-site term Hons, the interaction term Hint, and the electromagnetic term HEM:

\[ H = H_{\text{ons}} + H_{\text{int}} + H_{\text{EM}}. \]  

The on-site term is,

\[ H_{\text{ons}} = \sum_i \left( \Delta_s(s_i) + \sum_k \left( \hat{n}_k + \frac{1}{2} \right) \hbar \omega_k(s_i) \right) \]  

where \( \Delta_s(s_i) \) is the on-site term.
The FP-LAPW method\cite{23,24} an estimated Phase Approximation (cRPA)\cite{21,22} calculation using As a reference, we obtain from a constrained Random ground state energy is higher for the LS state.\cite{19} For the purpose of this work, it is necessary to tune $U$ to a value that can reproduce a reasonable LS-HS gap, at about 100 meV\cite{20}. We find that $U \approx 3.0 \sim 3.5$ eV.

As a reference, we obtain from a constrained Random Phase Approximation (cRPA)\cite{21,22} calculation using the FP-LAPW method\cite{23,24} an estimated $U \approx 3.2$ eV for Mn(3d) electrons in Mn(taa)\cite{25}.

The frequencies of the 159 phonon modes, including three translation modes and three rotation modes with zero frequency, are calculated for the isolated Mn(taa) in both LS and HS states. Certain phonon modes are softened in the HS state because one of the Mn-N bonds is elongated due to JT distortion, and correspondingly their occupation numbers are increased. Fig. 1(d)(e) show the results of differences of energy, free energy and entropy of phonon as a function of temperature by GGA-PBE and GGA+$U$. At zero temperature $T$, with zero vibration number for all phonon modes, the zero-point energy difference $E(h) - E(l)$ is -59.2 meV for PBE and varies between $-49.5 \sim -59.7$ meV for GGA+$U$ with $U = 2.5 \sim 3.5$, respectively. The phonon entropy is insensitive to $U$ and is larger for HS than LS, with the difference increasing with $T$.

The total entropy difference including both spin and phonon contributions causes the SCO to become a first-order phase transition\cite{2,26}. The transition temperature $T_c$ can be controlled by external strain\cite{27} and magnetic field\cite{25,28,29}. Although it was suggested that the phonon entropy does not dominate the phase transition on the basis of solid-state Raman spectra,\cite{15} a previous DFT study\cite{30} found that the phonon entropy difference in Mn(taa) is comparable to the spin-JT entropy difference, which is $k_B \ln(5 \times 3/3) = 13.8 J K^{-1} \text{mol}^{-1}$ at $T_c$. At $T_c = 45 K$, we calculate the phonon entropy difference to be $7.5 \sim 8.8 J K^{-1} \text{mol}^{-1}$.

Inter-molecular interactions arise from the elastic energy, which is treated classically because of the low vibration frequencies and high occupation numbers. Boukheddaden et al.\cite{31,32} suggested an isotropic elastic energy, which works well for many 1D and 2D lattice SCO systems. In the case of Mn(taa), because of the JT-active HS state, the strain interaction is anisotropic and depends on the shape of the molecules. Therefore, we assume an elastic energy of the form,

$$
H_{int} = \sum_{i,j} A_{s_i s_j} [(\mathbf{Q}(q_i) + \mathbf{Q}(q_j)) \cdot \hat{r}_{ij}]^2
$$

where $\mathbf{Q}$ is a dimensionless vector along the JT elongation axis so that $\mathbf{Q}(l,0) = (0,0,0)$, $\mathbf{Q}(h,x) = (1,0,0)$, $\mathbf{Q}(h,y) = (0,1,0)$, and $\mathbf{Q}(h,z) = (0,0,1)$. Each Mn(taa) molecule has five nearest neighbors. $\hat{r}_{ij}$ is the unitary direction between two neighbor sites $i$ and $j$. $A$ is the force constant in the dimension of energy and is a function of the spin-state $S$. We assume that in the LS state, two neighbor molecules are separated by the equilibrium distance with zero elastic energy, thus $A_{ll} = 0$. $A_{hh}$ is determined by the total energy difference between two HS bulk calculations with HS-Q$_{ab}$ and HS-Q$_c$, as indicated in Fig. 1(a). The plot in Fig. 1(c) shows that HS-Q$_c$ is always lower in energy than HS-Q$_{ab}$ so that the JT elongation axes of HS tend to align in parallel with each other. We find $A_{hh} = -10.0$ meV,
and to be insensitive to $U$. The negative sign indicates an effective anisotropic attraction caused by the JT distortion between two neighboring molecules.

The effects of magnetic field $H$, magnetic anisotropy $D$, and external electric field $E$ are given by $H_{EM}$:

$$H_{EM} = -\sum_i [\mu_0 H \cdot m_i + D (M(q_i) \cdot m_i)^2 + E \cdot P_i]$$  (4)

where $m$ is the magnetic moment determined by the magnetic quantum number $m$, and $P$ is the electric dipole on each site. In the LS state the three axes are equivalent so there is no anisotropy contribution. In the HS state, the magnetic easy axis is along the JT elongation axis. The magnetic anisotropic energy per molecule is 3.7 meV from first-principles, yielding $D \approx 0.3$ meV. In the Monte Carlo simulation, we assume that the magnetic moments are always aligned with $H$, which is in the $z$ direction. Thus the anisotropy energy only needs to be computed for sites with $q = 3$.

First principles calculations yield the magnitude $|P|$ of about 1.15 $e\text{Å}$ for both LS and HS states. In the LS state, the dipole moment directions of the molecules in the unit cell are shown in Fig. 2(a). Sixteen molecules belong to four groups, with the dipole directions in each group aligned along one of the four [111] directions. There is no net polarization in the unit cell. Once one molecule transitions to the HS state, an additional transverse dipole $P'$ of about 0.23 $e\text{Å}$ is created along the direction perpendicular to both its JT elongation axis and the original dipole direction, as shown in Fig. 2(b).

The first-order SCO phase transition as a function of $T$ in $\mu_0 H = 0$ is reproduced by Monte Carlo simulation using the microscopic Hamiltonian with the parameters obtained from first-principles calculations. The parameters are $\Delta = 74$ meV, $A_{hh} = -5.0$ meV, $A_{hl} = 5.0$ meV, and $D = 0.3$ meV. A small constant electric field of 0.1 mV/Å is applied along the $z$ direction. In Fig. 3 we show $\mu_0 H = 0$ specific heat $c_v$ (a), HS population $\rho_{HS}$ and HS sub-population for $q = 3$, $\rho_{HS-q3}$, and electric susceptibility $\chi_e$ (c) as a function of temperature. The first-order transition is clearly indicated by the singularity in the specific heat $c_v$ and the discontinuity in $\rho_{HS}$. $\rho_{HS-q3}$, and $\chi_e$ at the same $T$. $T_c$ averaged over cooling and heating is 44 K, matching experiments.[2, 26]

Now we are ready to examine the three HS phases by performing the simulations under different magnetic fields. The results are shown in Fig. 4. All four phases, LS, NP (HS non-polarized), FE (HS ferroelectric), and PE (HS paraelectric), are identified with phase boundaries (a) defined by the peaks in $c_v$, discontinuities in $\rho_{HS-q3}$ and the $z$ component of the electric polarization $P_z$. The LS phase is located at the low magnetic field and low temperature part of the phase diagram. The transition temperature approaches zero when the magnetic field reaches about 35 T. The PE phase is the high temperature HS phase with diminishing electric polarization. The NP and FE phases only exist under high magnetic fields.
The intermediate-temperature HS phase, labeled FE, has a non-zero net polarization. The snapshot of the FE phase unit cell in Fig. 4(d) shows one \( q = 0 \), three \( q = 1 \), nine \( q = 2 \) and 3 \( q = 3 \) molecules. Recall that \( q = 0 \) is the LS state. This means that the FE phase contains a small number of LS molecules. The sub-population of each JT axis is below its nominal value 1/3, also plotted in Fig. 4(f). This mixing of a small number of LS molecules naturally introduces disorder in JT ordering. Consequently the dipoles are no longer compensated. The electric susceptibility increases with increasing temperature and has a maximum at the transition temperature. This is a typical feature of ferroelectrics below the Curie temperature \([35]\). The thermal average polarization in this phase is about 0.02 mC/m\(^2\), smaller than that of one uncompensated dipole at a 10000 site. This strongly suggests that the nonzero polarization arises from dynamic fluctuation of the JT distortion, and that this intermediate phase is analogous to a liquid phase. Thus, we identify it as a JT liquid.

To understand the nature of the three JT phases, and to confirm that the intermediate phase indeed has liquid characteristics, we calculate the thermal average and the fluctuation of the nearest neighbor polarization correlation function \( \langle P'_{z,i}P'_{z,j} \rangle \), which are plotted in Figs. 4(i) and (j). The LS state without the JT degree of freedom has zero correlation and zero fluctuation in the low \( T \) region in \( \mu_0 H = 30 \) T. Among the three HS phases, the thermal average of the correlation for the NP and FE phases is much larger than for the PE phase, reflecting stronger correlation in the two lower temperature HS phases. On the other hand, fluctuation is higher for the two higher temperature HS phases, FE and PE, than the NP phase, besides the maximum at the phase transition boundary. The fluctuation in the FE phase is \( \sim 0.06 e^2 A^2 \) away from the phase boundary, much larger than the thermal average as \( \sim 0.01 e^2 A^2 \). In contrast, the fluctuation in the NP phase decays as \( T \) decreases due to the frozen JT degree of freedom. The dynamic behaviors can also be confirmed by the fluctuation in population [Fig. 4(h)]. \( \delta \rho_{HS} \) is equal to \( \delta \rho_{LS} \). The fluctuation \( \delta \rho_{LS} \) in the FE phase is larger than that in both LS and NP phases, indicating importance of the dynamics of the LS in the FE phase. \( \delta \rho_{HS-q_3} \) in the FE phase is also much larger than the corresponding thermal average. The above analysis reveals that the FE phase exhibits correlated and dynamic JT distortion. Correlation and dynamic fluctuation are properties generally identified with a liquid in condensed matter.

In summary, we introduced a molecular-scale Hamiltonian to describe the SCO system Mn(taa) with parameters obtained from first principles calculations. Monte Carlo simulations using this Hamiltonian qualitatively reproduce the experimental phase diagram and yield microscopic understanding of the observed
phases. The strain interaction is the primary factor controlling the ordering and dynamics of JT distortions, producing three JT states of matter (JT solid, JT liquid, and JT gas) in different magnetic fields and temperatures. The JT liquid is particularly interesting because of the dynamic JT fluctuation in this phase and the uncompensated electric polarization. Disorder and dynamic JT fluctuation are quite common in spin-crossover materials. Thus one may expect JT liquid to be discovered in other systems.

This work was supported as part of the Center for Molecular Magnetic Quantum Materials, an Energy Frontier Research Center funded by the U.S. Department of Energy, Office of Science, Basic Energy Sciences under Award No. [de-sc0019330]. Computations were done using the utilities of National Energy Research Scientific Computing Center, the Extreme Science and Engineering Discovery Environment under No. TG-PHY170023 and University of Florida Research Computing systems.

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