Rotor Spacing and Blade Number Effect on the Thrust, Torque, and Power of a Coaxial Rotor

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Received/Geliş: 16.12.2019

Accepted/Kabul: 27.02.2020

Abstract: In this study, rotors space and number of the blade are examined in terms of the torque, power and thrust concept. Three-dimensional flow analysis was performed by using SolidWorks flow simulation. In aircraft propeller design, thrust, torque and power concept has a great deal of importance. The rotor can be defined as a propulsion system, which provides the thrust with a propeller. The pressure difference produces due to the velocity difference between the lower and upper surfaces of the airfoil. The thrust is obtained with this pressure difference. The rotor blades produce drag and thrust thanks to rotating airfoils. The number of the blade affects the amount of thrust directly. If the blade number of rotor increases, the produced thrust, torque by the rotor and the needed power to drive rotor will also increase. In this study, the effect of blade number (2, 3 and 4 blades) and distance between rotors (0.05*D, 0.1*D, 0.25*D, 0.5*D, 0.75*D, 1*D) on the thrust, torque and power are investigated.

Keywords: Rotor, CFD, Power, Thrust, Torque

1. Introduction

A rotor is a type of fan that transmits power by converting rotational motion into thrust. A pressure difference is produced between the forward and rear surfaces of the airfoil-shaped blade, and a fluid (such as air or water) is accelerated behind the blade. Rotor dynamics, like those of aircraft wings, can be modeled by either or both Bernoulli’s principle and Newton's third law [1]. Rotors are the most critical parts for the propulsion systems. In the literature, nearly all studies are focused on marine propellers. There are few studies that exist about aero propellers. Noh et al. [2] investigated...
different angles of attack values (25°, 35°, and 45°) effect on the airfoil and flat shape louvers. The symmetrical 4-digit NACA airfoil shape was used as louvers and it had 10 mm thickness. Solid Works Flow Simulation tool was used for CFD analysis. The results show that pressure drop is more widespread in flat louvers as compared to airfoil louvers. Hong and Dong [3] was presented a process for numerical analysis of the radial circulation distribution of the rotor blade. This process is based on the results of numerical simulation of the velocity field around rotor blades and in the wake. A method to estimate full-scale rotor torque and thrust consisting of low-frequency and high-frequency components in waves by a free-running model ship test were proposed by Ueno and Tsukada [4]. Driss et. al. [5] applied an experimental validation and numerical simulation to study the turbulent flow around a small incurved Savonius wind rotor. For the analysis, the Solid Works flow simulation tool was used. Navier-Stokes equations and standard k-ε turbulence model were used. These equations were solved by a finite volume discretization method. The effect of the ducted fan, which is located inside the ground effect region, is investigated experimentally according to the helicopter hovering concept by Doğru et. al. [6]. For this investigation, the thrust of the ducted fan is measured using two different experimental methods, which are static pressure measurement system and spring method to calculate the thrust. Lei et. Al. [7] studied on performance of a coaxial rotor. They used thrust and power consumption as performance parameters of the system and rotor spacing and wind speed as design parameters. Göv [8] investigated thrust, torque and power concepts according to different blade numbers (2, 3 and 4 blades). Yoon et. al. [9] investigated the effects of torque balancing on the performance of coaxial-rotor systems. Han et. al. [10] developed an efficient hybrid inverse/optimization design method that combines inverse design and direct optimization within a surrogate-based optimization (SBO) framework for rigid coaxial rotor airfoils considering reverse flow. Kavuran et. al. [11] developed an experimental test platform of a low-cost coaxial rotor for implementation of Model Reference Adaptive Controller (MRAC) with Fractional Order Adjustment Rules by using MATLAB/Simulink. Shukla and Komerath [12] investigated the interactions between wakes of two side-by-side rotors as a function of the distance between the rotors and their Re at from instantaneous as well as mean flow field perspective. Feil et. al. [13] developed a comprehensive analysis model of a laboratory-scale torque-balanced rotor designed for high-advance-ratio forward flight to investigate the aeromechanics of coaxial counter-rotating lift-offset rotor systems. Gül and Kolip [14] studied to increase the wing performance by reducing the reverse resistance in the convex blade of the Savonius wind turbine, which is a vertical axis wind turbine. Chen at. al. [15] presented a mechanical configuration of an independent pitch control system (IPCS) for a coaxial dual-rotor compound helicopter (CDCH), which is mainly constituted by parallel mechanism, spatial orientation, lower rotor, and upper rotor. Jiang et. al. [16] adopted Multiblock grids and Multiple Frame of Reference model to predict the complex viscous flow of multirotor, which transforms the time-dependent formulation into a steady-state approximation. The predictive capability of the new configuration as well as the SUAV was very high and validated by the experimental results. Yuan et. al. [17] proposed a coaxial compound configuration as a concept for future high-performance rotocraft. Ferguson and Thomson [18] investigated the compounding of the conventional helicopter and how the addition of thrust and wing compounding influences the performance of this aircraft class. Santos-Medina et. al. [19] discussed the design and modeling of a spherical flying robot to control its hovering and omnidirectional mobility by controlling the air mass differential pressure between two asynchronous coaxial rotors that are aligned collinearly. Kim et. al. [20] investigated the aerodynamics and acoustics of a generic coaxial helicopter with a stiff main rotor system and a tail-mounted propulsor using Brown’s Vorticity Transport Model. Enconniere et. al. [21] presented the development and application of a multidisciplinary methodology for the preliminary design assessment of compound coaxial rotocraft with a counter-rotating rotor system and a rear-mounted propeller. Enconniere et. al. [22] presented the performance analysis of a coaxial counter-rotating rotor configuration with a pusher propeller to quantify the benefits of compound rotocraft. Lyu and Xu [23] established a comprehensive
calculation model of a counter-rotating coaxial-rotor propeller-augmented compound helicopter based on the free-wake method to investigate its interactional aerodynamic characteristics.

After the literature review, it is seen that many studies are focused on marine propellers. There are few studies that exist about aero propellers. Also, the effect of the rotor distance and blade number on the performance of the coaxial rotor is not investigated in any study.

There are three theories used in the design of propellers. They are blade element, momentum, and vortex theory. Most of today’s propellers are designed using blade element theory.

Induced velocity (eq. 1) and power (eq. 2) equations for coaxial rotors are given below:

\[
(v_i)_e = \frac{(2\pi)}{\sqrt{2 \rho A}}
\]

\[
(P_i)_{tot} = 2T(v_i)_e = \frac{(2\pi)^{1/2}}{\sqrt{2 \rho A}}
\]

If each rotor taken as separately the induced power (eq. 3) for each rotor is \( T v_i \) and the sum of two is:

\[
P_i = 2 \times \frac{T^{1/2}}{\sqrt{2 \rho A}}
\]

Calculating the interference-induced power factor (eq. 4):

\[
K_{int} = \frac{(P_i)_{int}}{P_i} = \left[\frac{2\pi^{1/2}}{\sqrt{2 \rho A}}\right] / \left[\frac{2\pi^{1/2}}{\sqrt{2 \rho A}}\right] = \sqrt{2}
\]

Coaxial rotor increase of 41% in the induced power [7].

2. CFD Analysis

In this study, a numerical calculation method with the SolidWorks flow simulation tool is used for cases. A standard rotor is used in numerical calculations. In the numerical study, the external flow type is used (Figure 1). In addition, “exclude cavities without flow conditions” and “exclude internal space” are selected since the present study is not interested in cavities or spaces.

NACA 0012 airfoil is used to obtain the rotor as shown in Figure 2. In the numerical study 2 blades (in Figure 3), 3 and 4 blades (in Figure 4) rotors are used. 660 mm Rotor diameter is used for all rotors. Different rotor distances are investigated according to D which is rotor diameter as 0.05D, 0.1D, 0.25D, 0.5D, 0.7D, and 1D. Optimum rotor distance was obtained according to numerical results.

Air is defined as the fluid domain for the environment of the system as shown in Figure 5. Also, the Rotational domain is created as shown in Figure 6.
Figure 1. Coaxial rotor Flow Representation [7]

Figure 2. Blade airfoil [24]

Figure 3. Front and side view of 2 blades rotor

Figure 4. Front view of 3 blades and 4 blades rotors
Initial conditions are defined as: there is no velocity in any direction because there is no crosswind. Temperature is assumed to be room temperature (20° C) on the atmospheric pressure. This numerical study was performed at the 2500 RPM (261.71 rad/s).

The rotational region is covered with the environmental pressure to simulate the real conditions after the boundary conditions are defined. The element number effect is researched and the result is...
given in Figure 7. As a result of this research, approximately 470000 element number is used in the analyses.

2. **Results and Discussion**

In this study, rotor thrust and torque values are calculated at different blade numbers and different rotor spacing values by using the SolidWorks flow simulation analysis program. Also, pressure distribution (in Figure 8) and velocity distribution (in Figure 9) are calculated for 0.05*D (33mm) rotor spacing. Flow distribution, tip flow distribution and flow lines are given in figures 10, 11 and 12 respectively for 0.05*D (33mm) rotor spacing.

![Figure 8. Pressure distribution of coaxial rotor at 0.05*D rotor spacing](image)

![Figure 9. Velocity distribution of coaxial rotor at 0.05*D rotor spacing](image)

![Figure 10. Flow distribution of coaxial rotor at 0.05*D rotor spacing](image)
Figure 11. Tip flow distribution of coaxial rotor at 0.05*D rotor spacing

Figure 12. Flow lines of the coaxial rotor at 0.05*D rotor spacing

Pressure distribution (in Figure 13) and velocity distribution (in Figure 14) are calculated for 0.5*D (330mm) rotor spacing. Flow distribution, tip flow distribution and flow lines are given in figures 15, 16 and 17 respectively for 0.5*D (330mm) rotor spacing.

Figure 13. Pressure distribution of coaxial rotor at 0.5*D rotor spacing

Figure 14. Velocity distribution of coaxial rotor at 0.5*D rotor spacing
Figure 15. Flow distribution of coaxial rotor at 0.5*D rotor spacing

Figure 16. Tip flow distribution of coaxial rotor at 0.5*D rotor spacing

Thrust and torque values are calculated from the analysis program for the 2 blades single rotor as shown in Table 1.

| 2 Blades | Averaged Value |
|----------|----------------|
| Thrust (N) | 10.3 |
| Torque (N*m) | 0.77 |
| Power (watt) | 201.75 |
| Thrust/Power | 0.051 |
Figure 17. Flow lines of the coaxial rotor at 0.5*D rotor spacing

Thrust and torque value are calculated from the analysis program for the 3 blades single rotor as shown in Table 2.

| 3 Blades | Averaged Value |
|----------|----------------|
| Thrust (N) | 14.55 |
| Torque (N*m) | 0.99 |
| Power (watt) | 259.39 |
| Thrust/Power | 0.056 |

Table 2. Results of 3 blades single rotor

Thrust and torque value are calculated from the analysis program for the 4 blades single rotor as shown in Table 3.

| 4 Blades | Averaged Value |
|----------|----------------|
| Thrust (N) | 16.86 |
| Torque (N*m) | 1.33 |
| Power (watt) | 348.47 |
| Thrust/Power | 0.048 |

Table 3. Results of 4 blades single rotor

Thrust value with respect to rotor spacing of 2 blades coaxial rotor is given in figure 18. And torque value with respect to rotor spacing of 2 blades coaxial rotor is given in Figure 19.
Thrust value with respect to rotor spacing of 3 blades coaxial rotor is given in Figure 20. And torque value with respect to rotor spacing of 3 blades coaxial rotor is given in Figure 21.
Figure 21. Torque results of 3 blades rotor

Thrust value with respect to rotor spacing of 4 blades coaxial rotor is given in Figure 22. And torque value with respect to rotor spacing of 4 blades coaxial rotor is given in Figure 23.

Figure 22. Thrust results of 4 blades rotor

Figure 23. Torque results of 4 blades rotor

A comparison of the thrust values of the upper rotor for different blade numbers is given in Figure 24.
Figure 24. Thrust results of the upper rotor

A comparison of the thrust values of the lower rotor for different blade numbers is given in Figure 25.

Figure 25. Thrust results of the lower rotor

A comparison of torque values of the upper rotor for different blade numbers is given in Figure 26.

Figure 26. Torque results of the upper rotor

A comparison of torque values of the lower rotor for different blade numbers is given in Figure 27.
A comparison of the power values of the upper rotor for different blade numbers is given in Figure 28.

A comparison of the power values of the lower rotor for different blade numbers is given in Figure 29.
Comparison of thrust/power ratio of the upper rotor, lower rotor and total is given in Figure 30, Figure 31 and Figure 32 respectively.

3. Conclusions
In this study, rotor spacing and blade number of rotor concepts are investigated. Within this scope, thrust, torque and power values of the rotor, which have different blade numbers (2, 3 and 4 blades) are examined. The CFD analysis is used to perform the suggested study. The velocity and pressure distribution are obtained according to boundary and flow conditions. The maximum tip velocity is obtained by nearly 112.67 m/s for all rotors. As can be understood from the obtained speed value, the tip speed of the rotors does not exceed the speed of sound. Power value increased in proportion to the number of blades. It has been observed that the amount of increase in thrust is low in 3-blade rotor compared to the number of 2 blades, but there is more increase in 4-blade rotor compared to 2 and 3-blade rotor. It was found that the torque value in the lower rotor is higher due to the pressure difference between the lower rotor and the upper rotor. At the end of the study, it was determined that the torque value is increasing linearly with respect to the blade number. But, thrust value does not increase linearly as torque value. This means that the power requirement is increasing non-linearly due to blade number.

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