Stringent constraint on the radio signal from dark matter annihilation in dwarf spheroidal galaxies using the TGSS

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ABSTRACT

Weakly Interacting Massive Particles (WIMPs) are considered to be one of the favoured dark matter candidates. Searching for any detectable signal due to the annihilation and decay of WIMPs over the entire electromagnetic spectrum has become a matter of interest for the last few decades. WIMP annihilation to Standard Model particles gives rise to a possibility of detection of this signal at low radio frequencies via synchrotron radiation. Dwarf Spheroidal Galaxies (dSphs) are expected to contain a huge amount of dark matter which makes them promising targets to search for such large scale diffuse radio emission. In this work, we present a stacking analysis of 23 dSph galaxies observed at low frequency (147.5 MHz) as part of the TIFR-GMRT Sky Survey (TGSS). The non-detection of any signal from these stacking exercises put very tight constraints on the dark matter parameters. The best limit comes from the novel method of stacking after scaling the radio images of the individual dSph galaxy fields after scaling them by the respective half-light radius. The constraint on the thermally averaged cross-section is below the thermal relic cross-section value over a range of WIMP mass for reasonable choices of relevant astrophysical parameters. Such analysis using future deeper observation of individual targets as well as stacking can potentially reveal more about the WIMP dark matter properties.

Key words: galaxies: dwarf – dark matter – diffuse radiation – radio continuum: galaxies

1 INTRODUCTION

The hierarchical structure formation model predicts existence of numerous low mass satellite galaxies gravitationally bound to larger, high mass galaxies. For the Milky Way (and the local group), a large fraction of these observed satellite galaxies are dwarf spheroidal (dSph) galaxies. The dSph galaxies, very similar to the globular cluster population, are gravitationally bound, diffuse, low surface brightness and low luminosity systems (Strigari et al. 2008a), with low metallicity and old stellar population (McConnachie 2012), and having negligible gas and dust content, as well as very little or no recent star formation. However, unlike the globular clusters, they have very high dynamical mass to light ratio (Sparke & Gallagher 2016), indicating that they are dark matter (DM) dominated systems (e.g. Strigari et al. 2008a,b). The presence of dark matter can also be inferred from the kinematics studies of dSph galaxies (e.g. Bosma & van der Kruit 1979; Rubin et al. 1980). Based on a variety of observations, the dSph galaxies are thought to be the most dark matter dominated systems, and hence are considered to be among the most promising targets for the indirect detection of dark matter (Strigari 2018).

One of the proposed scenarios for indirectly detecting the DM signal is to look for the standard model annihilation/decay products, and the corresponding excess signature in the electromagnetic spectra. A specific case of interest is the weakly interacting massive particles (WIMPs) as DM candidate: here the DM annihilation producing electron-positron pairs through various interaction and decay channels. These charged particles, in turn, can produce broadband electromagnetic emission like bremsstrahlung, inverse Compton, and, particularly at low radio frequency range, synchrotron emission in presence of the, albeit weak, galactic magnetic field Colafrancesco et al. (2007); Profumo & Ullio (2010). Although this signal is expected to be very faint, as the dSph galaxies otherwise have very little or no diffuse low radio frequency emission, due to their expected high DM fraction and their relative proximity, it is in principle possible to detect (or put stringent limit on) this signal, and in turn constrain or rule out certain models on the nature of DM from such observations. Another promising avenue is to look for an excess γ-ray signal arising due to DM annihilation. Several recent studies have explored this avenue and find some important clues on...
the GMRT allow identification and subtraction of compact sources (GMRT). The unique array configuration and high sensitivity of the GMRT implies that the telescope half-light radius distribution is shown in Fig. 1. Note that the unique hybrid array configuration of the GMRT has sensitivity to both small scale compact structures as well as large scale diffuse emission, with the largest detectable structure (corresponding to the shortest baselines) being 68 arcmin. If the diffuse emission from these targets have angular extent ~ few $r_h$, there will not be any significant missing flux issue in this analysis.

3 DATA ANALYSIS

For the 23 dSph galaxies, we have used the TGSS-ADR1 image archive to extract the image of a region centred around the optical position of each of the galaxies in FITS format combining data from multiple overlapping TGSS pointing. For the first part of our analysis, we have extracted $1^{\circ} \times 1^{\circ}$ region for each of the target dSph galaxies. Further analysis was done using the Common Astronomy Archive Tagging System (CAST) and the HiPercam Pipeline (HPP) to generate the images.

We first attempt to find evidence of diffuse synchrotron emission from the dark matter. A similar study by Vollmann et al. (2020) using LOFAR observations is also consistent with null detection. The results are mostly limited by the low sensitivity and Galactic foreground contamination. Based on the observed limit, they put some constraints on the magnetic field strength as well as DM parameters, e.g., the halo density profile (Navarro et al. 1996; Spekkens et al. 2013) and the degree of diffusion. Recently, Kar et al. (2020) have also used deep (58 mJy beam$^{-1}$) MWA observation of $\omega$ Centauri at 200 MHz and best fit values of DM particle mass and annihilation cross section from $\gamma$-ray observations (Brown et al. 2019) to rule out significant parts of the magnetic field - diffusion coefficient plane.

In this paper we present an analysis for 23 dSph galaxies using the 150 MHz data from the Giant Metrewave Radio Telescope (GMRT). The unique array configuration and high sensitivity of the GMRT allow identification and subtraction of compact sources and, at the same time, constraining the large scale diffuse emission with ~ 1' resolution. The paper is organized as follows. The DSp

\begin{table}
\centering
\begin{tabular}{lcccc}
\hline
Name & R.A. & Dec. & $r_h$ (') & D (kpc) \\
\hline
Aquarius & 20h46m52s & $-12^\circ50'33''$ & 1.47 $\pm$ 0.04 & 1072 $\pm$ 39 \\
Bootes I & 14h00m16s & $+4^\circ36'00''$ & 12.6 $\pm$ 1 & 66 $\pm$ 2 \\
Bootes II & 13h58m00s & $+42^\circ15'00''$ & 4.2 $\pm$ 1.4 & 42 $\pm$ 1 \\
Carina & 06h41m37s & $-50^\circ57'38''$ & 8.2 $\pm$ 1.2 & 105 $\pm$ 6 \\
Cetus & 00h26m11s & $-11^\circ02'40''$ & 3.2 $\pm$ 0.1 & 755 $\pm$ 24 \\
Columbia I & 05h31m26s & $-28^\circ01'48''$ & 1.9 $\pm$ 0.5 & 182 $\pm$ 18 \\
Draco & 17h20m12s & $+57^\circ54'55''$ & 10.0 $\pm$ 0.3 & 76 $\pm$ 6 \\
Fornax & 02h39m59s & $-34^\circ24'57''$ & 16.6 $\pm$ 1.2 & 147 $\pm$ 12 \\
Grus I & 22h56m42s & $-50^\circ09'48''$ & 1.77 $\pm$ 0.35 & 127 $\pm$ 6 \\
Grus II & 22h04m05s & $-46^\circ26'24''$ & 6.0 $\pm$ 0.7 & 53 $\pm$ 5 \\
Hercules & 16h31m02s & $+12^\circ47'30''$ & 8.6 $\pm$ 1.1 & 132 $\pm$ 12 \\
Hydra II & 12h21m42s & $-31^\circ59'07''$ & 1.7 $\pm$ 0.3 & 134 $\pm$ 10 \\
Leo I & 10h08m28s & $+12^\circ18'23''$ & 3.4 $\pm$ 0.3 & 254 $\pm$ 15 \\
Leo II & 11h13m29s & $+22^\circ09'06''$ & 2.6 $\pm$ 0.6 & 233 $\pm$ 14 \\
Leo IV & 11h32m57s & $-00^\circ32'00''$ & 4.6 $\pm$ 0.8 & 154 $\pm$ 6 \\
Leo V & 11h31m10s & $+02^\circ13'12''$ & 2.6 $\pm$ 0.6 & 178 $\pm$ 10 \\
Phoenix & 01h51m06s & $-44^\circ26'41''$ & 3.76 & 415 $\pm$ 19 \\
Sagittarius II & 19h52m40s & $-22^\circ04'05''$ & 2.0 $\pm$ 0.4 & 67 $\pm$ 5 \\
Sculptor & 01h00m09s & $-33^\circ42'33''$ & 11.3 $\pm$ 1.6 & 86 $\pm$ 6 \\
Segue II & 02h19m16s & $+29^\circ10'31''$ & 3.4 $\pm$ 0.2 & 35 $\pm$ 2 \\
Ursa Major II & 08h51m30s & $+63^\circ07'48''$ & 16 $\pm$ 1 & 32 $\pm$ 4 \\
Ursa Minor & 15h09m09s & $+67^\circ13'21''$ & 8.2 $\pm$ 1.2 & 76 $\pm$ 3 \\
Willman I & 10h49m22s & $+51^\circ03'03''$ & 2.3 $\pm$ 0.4 & 38 $\pm$ 7 \\
\hline
\end{tabular}
\caption{List of the dwarf spheroidal galaxies used in this analysis, with their J2000.0 coordinates, half-light radius ($r_h$) and distance (D).}
\end{table}
Software Applications (CASA) package. We have visually inspected each field to identify and blank all the compact sources (unresolved and marginally resolved) using a 5σ cut off. These compact sources are unrelated to the expected faint diffuse emission (originating from processes directly involving the DM annihilation/decay) at the galaxy-wide scale, that is of our interest. This will also filter out any plausible unidentified imaging artifact present in the field. We then shift the central coordinate of all the fields, regrid and convolve the data to exactly same pixel size and same synthesized beam before combining to create a stacked image from all 23 dSph target field. We have also selected 23 “control” regions, located close to the corresponding target field regions, that are devoid of any prominent sources. The same process is repeated for these regions to create a stacked image of the control field. We have then compared the properties of the stacked target and control field to search for the presence of any weak, extended emission signal (see §4).

For the second part of our analysis, instead of stacking a fixed angular size of $1^\circ \times 1^\circ$, we have used the half-light angular radius ($r_h$) of the dSph galaxies to scale the individual regions before stacking. For this, we start by extracting a subimage of $3r_h \times 3r_h$ for each source. The same steps of removing the compact sources, scaling, regridding and convolving to the same synthesized beam were followed to create the stacked image from the target regions. As earlier, exactly same method was followed to create a stacked image of the control field as well. The results of a careful comparison between the stacked target and control field are presented in the following section.

4 RESULTS AND DISCUSSION

4.1 Comparison between target and control regions

Fig. 2 shows the final $1^\circ \times 1^\circ$ stacked target (left) and control (right) regions obtained using the first method described in section 3. As described earlier, the stacking is done after removing all prominent compact sources from individual fields. Even after stacking, no significant large scale emission is visually prominent in either the target field or the control field. The final RMS noise is $\sim 4$ mJy beam$^{-1}$ (with a beam size of 75.6") for both target and control regions. For comparison, the stacked image for the GLEAM survey had a synthesized beam of size 2.28′ with the RMS sensitivity 5.5 mJy beam$^{-1}$. We note that the mean values ($0.11$ mJy beam$^{-1}$ for target field and $0.13$ mJy beam$^{-1}$ for control field) are consistent with each other within the error values. A more quantitative comparison between the intensity distributions of the target and control field, shown in Fig. 3 left panel, is also done. We have used the non-parametric Kolmogorov-Smirnov (K-S) test with the pixel intensity values (after regridding to 37 arcsec); based on the K-S $D$ statistics values ($D = 0.016$ and the $p$-value 0.16), we conclude that the stacked target and control images intensity distributions are likely to be very similar. The radial intensity profiles (mean surface brightness in different radial bins, and measured RMS in each bin) shown in the right panel of Fig. 3 shows the two stacked images to also have indistinguishable profiles within the statistical uncertainties.

Apart from the mean and the distribution function of the intensity values, we have also compared the second order statistics by estimating the angular power spectra of the intensity fluctuations. We convert the image in the Fourier domain using the Fastest Fourier Transform in the West (FFTW; Frigo & Johnson 2005) and calculate the angular power spectrum. We also multiply the image with a cosine window function to avoid artifacts arising due to the sharp cut-off at the edge (Miville-Deschênes et al. 2016; Choudhuri & Roy 2019). As shown in Fig. 4, the angular power spectrum of the stacked target and the control regions are same within the measurement uncertainty. We note that over the $U$ range of 5 to 30 deg$^{-1}$ (i.e., $\sim 2^\prime$ to $12^\prime$), the power spectra can be well represented by a power law with a power law index of $-1.82 \pm 0.05$ and $-2.05 \pm 0.09$ for the target and the control region respectively. We choose this $U$ range because $U < 5$deg$^{-1}$ the power spectrum is convolved with the Fourier transform of the window function, and $k > 30$deg$^{-1}$ the image is convolved with the synthesized beam. These measured slopes of the angular power spectrum are consistent with earlier power spectra measurements of the diffuse Galactic synchrotron emission (Bernardi et al. 2009; Ghosh et al. 2012; Iacobelli et al. 2013; Choudhuri et al. 2017; Chakraborty et al. 2019). Apart from an overall consistency check, this result clearly indicates that the TGSS data are suitable to probe diffuse emission at large angular scale, similar to the expected radio signal associated with the DM halo of the dSph galaxies, present in the field.

Next, we consider results from a novel stacking method after...
scaling the radio images of individual dSph fields by the respective half-light angular radius $r_h$. Here, we have assumed that the large scale diffuse signal that we are searching for has characteristic angular scale related to the optical half-light radius ($r_h$). In absence of any direct estimation of the DM halo size of the sample galaxies, this is a reasonable assumption. If that is indeed the case, then, by scaling all the images using the respective $r_h$ and stacking the images, the expected radio emission profiles align with each other and the stacked signal is more likely to be detected. After following the steps described earlier in §3, i.e. blanking compact sources, scaling and regridding the images, convolving to a common synthesized beam and stacking, the final images for the target and the control field are shown in the top panels of Fig. 5. For the two stacked images, the mean values are 0.57 mJy beam$^{-1}$ and 0.84 mJy beam$^{-1}$ and the rms values are 16 mJy beam$^{-1}$ and 11 mJy beam$^{-1}$, with the final convolving beam size of 0.69 in $r_h$ unit, for the target and the control fields respectively.

One limitation of the analysis with $r_h$ scaling is that the final stacked images have poor resolution. The images are convolved to the same Gaussian beam before stacking, and the resolution is determined by the target with smallest $r_h$ in angular size. We hence also repeat the same analysis for a subsample of 11 targets with $r_h > 4'$. The final stacked images of the target and the control fields are shown in the bottom panels of Fig. 5. For a final convolving beam of 0.17 in $r_h$ unit, the mean values are 0.9 mJy beam$^{-1}$ and 0.5 mJy beam$^{-1}$ where as the rms values are 10 mJy beam$^{-1}$ and 9 mJy beam$^{-1}$, respectively.

For the “$r_h$-stacking” also, we have carried out the similar comparison of the intensity distributions, the radial intensity profiles and the angular power spectra for both the subsample and the full sample. The target and the control region have statistical properties consistent with each other within the measurement uncertainties ($D = 0.095$ and $p = 0.44$ for the full sample and $D = 0.032$ and $p = 0.13$ for the sub-sample in K-S test, indicating very similar distribution of intensities for the stacked target and control image). As shown in Fig. 6, there is indication of possible slight excess in the radial profile, however significantly higher sensitivity data are required to check if the feature is real. Overall, the results are consistent with no detection of diffuse large scale signal, and we put some stringent constraints on the galaxy scale diffuse emission at low radio frequency from the dSph galaxies.

### 4.2 Constraints on dark matter

Based on the non-detection of diffuse low frequency emission in these stacking exercises, one can put constraints on DM parameters under reasonable assumptions for the astrophysical conditions in dSph galaxies. This is done by first evaluating the equilibrium electron positron spectra considering diffusion equation (where the source term depends on the DM particle cross-section and mass), and then computing the expected signal for the frequency range of interest due to different emission mechanism (see, e.g., Nataraajan et al. 2013; Colafrancesco et al. 2006; Storm et al. 2017; Colafrancesco et al. 2007; Beck & Colafrancesco 2016; McDaniel et al. 2017; Geringer-Sameth et al. 2015; Kar et al. 2020, for more details). A comparison of the expected and observed signal (or the upper limit in case of non-detection) can then constrain the DM particle mass and cross-section.

For the purpose of deriving the constraints from these observations, publicly available package RX-DMFIT (McDaniel et al. 2017) has been used. We choose a very conservative 5σ upper limit of the estimated flux density at 147.5 GHz for these computations. The signal is computed for an archetypal dSph galaxy for our sample (similar to the Draco dwarf spheroidal galaxy with core radius 0.22 kpc and radius for diffusion effect 2.5 kpc) placed at a distance
Figure 5. Top: Stacked images of the target (left) and the control region (right) for a sample of 23 dSph galaxies. Bottom: Same for a subsample of 11 galaxies with $r_h > 4'$. The grey scale unit is Jy beam$^{-1}$, where the beam size is 0.69 and 0.17 in $r_h$ unit for the top and the bottom panels, respectively.

Figure 6. Radial intensity profile for the stacked target and control region when scaled by half-light radius, $r_h$, for a sample of 23 dSph galaxies (left), for a subsample of 11 galaxies with $r_h > 4'$ (right).

of 129.5 kpc, which the median distance for our sample. We also choose $B = 2 \mu$G, and diffusion coefficient $D_0 = 3 \times 10^{26}$ cm$^2$s$^{-1}$ (Kar et al. 2019; Natarajan et al. 2015, 2013; Jeltema & Profumo 2008; Regis et al. 2015; Chyży et al. 2011) as fiducial parameters. As shown in Fig. 7, we get the best constraint on the average cross-section $\langle \sigma v \rangle$ for different DM mass ($M_\chi$) for the 5$\sigma$ flux density limit of 0.17 Jy from the “$r_h$ stacking” (solid lines in all three panels). The constraints are shown for three different channels, namely $b\bar{b}$, $\mu^+\mu^-$ and $\tau^+\tau^-$ (see McDaniel et al. 2017, for details). The cross-section values are shown for a WIMP mass range of 1 – 1000
Figure 7. Constraints on DM particle mass ($M_D$) and cross-section ($\langle\sigma v\rangle$) for three different channels - $bb$ (blue), $\mu^+\mu^-$ (green) and $\tau^+\tau^-$ (red). Solid lines in all three panels are for the 5σ flux density limit from the “r$_h$ stacking”, $B = 2$ μG and $D_0 = 3 \times 10^{26}$ cm$^2$s$^{-1}$. The dot-dash lines are using 5σ flux density limit from the 1$\times$1$'$ stacking (left panel), $B = 1$ μG (top right panel), and $D_0 = 3 \times 10^{25}$ cm$^2$s$^{-1}$ (bottom right panel). The thermal relic cross-section value is marked by solid black line. The current best limits from Fermi-LAT gamma ray observations (Hoof et al. 2020b) for the corresponding decay channels are also shown in dashed lines in the left panel for comparison.

5 CONCLUSIONS

Detection of diffuse radio emission from dSph galaxies can be a smoking gun evidence for WIMP as possible dark matter candidate. Apart from straightforward stacking, we have also tried a novel method of scaling the radio images by the corresponding $r_h$ of the respective dSph galaxies followed by stacking to get a deeper limit on the average flux density from this sample. However, over a range of scale probed in this analysis $U \sim 5 - 30$ deg$^{-1}$, the angular power spectra are found to be power law, with the best fit power law index being consistent with earlier measurements of the diffuse Galactic synchrotron emission. Based on the non-detection of any detectable excess radio emission, we have put tight limits on the thermally averaged cross-section for WIMP mass range of 1 – 1000 GeV under the assumption of some reasonable astrophysical conditions. With our choices of the parameters, the cross section limit over a significant fraction of the DM mass range is below the thermal relic cross-section limit for $bb$, $\mu^+\mu^-$ and $\tau^+\tau^-$ channels. It should be noted that the current analysis is limited by the sensitivity due to the small on-source time per field for the TGSS images. Hence, application of the this method of “r$_h$ stacking” with deeper images of the targets from future observations can further improve the limits. Also, combining such observations for larger sample and over the electromagnetic spectrum to put joint limits will also push the constraints. Finally, upcoming telescopes like the Square Kilometre Array (SKA) will have the sensitivity to detect this radio signal or to put orders of magnitude better limits.

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DATA AVAILABILITY

The data used for this study is available from the TGSS ADR image archive (data release 1). The final data products from this study will be shared on reasonable request to the corresponding author.

REFERENCES

Ackermann M., et al., 2015, Phys. Rev. Lett., 115, 231301
Archambault S., et al., 2017, Phys. Rev. D, 95, 082001
Beck G., Colafrancesco S., 2016, J. Cosmology Astropart. Phys., 2016, 013
Bernardi G., et al., 2009, A&A, 500, 965
Bhattacharjee P., Majumdar P., Biswas S., Joarder P. S., 2019, J. Cosmology Astropart. Phys., 2019, 028
Biswas S., Bhattacharjee P., Majumdar P., Das S., Das M., Joarder P. S., 2017, J. Cosmology Astropart. Phys., 2017, 003
Rosma A., van der Kruit P. C., 1979, A&A, 79, 281
Brown A. M., Massey R., Lacroix T., Strigari L. E., Fattahi A., Bœhm C., 2019, arXiv e-prints, p. arXiv:1907.08564
Chakraborty A., et al., 2019, MNRAS, 487, 4102
Charbonnier A., et al., 2011, MNRAS, 418, 1526
Choudhuri S., Roy N., 2019, MNRAS, 483, 3437
Choudhuri S., Bharadwaj S., Ali S. S., Roy N., Intema H. T., Ghosh A., 2017, MNRAS, 470, L11
Chyż K. T., Weżgowiec M., Beck R., Bomans D. J., 2011, A&A, 529, A94
Colafrancesco S., Profumo S., Ullio P., 2006, A&A, 455, 21
Colafrancesco S., Profumo S., Ullio P., 2007, Phys. Rev. D, 75, 023513
Cook R. H. W., et al., 2020, MNRAS, 494, 135
Drlica-Wagner A., et al., 2020, ApJ, 893, 47
Frigo M., Johnson S. G., 2005, Proceedings of the IEEE, 93, 216
Geringer-Sameth A., Koushiappas S. M., Walker M., 2015, ApJ, 801, 74
Ghosh A., Prasad J., Bharadwaj S., Ali S. S., Chengalur J. N., 2012, MNRAS, 426, 2925
Hoof S., Geringer-Sameth A., Trotta R., 2020a, Supplementary Material for A Global Analysis of Dark Matter Signals from 27 Dwarf Spheroidal Galaxies using 11 Years of Fermi-LAT Observations, https://doi.org/10.5281/zenodo.2612268
Hoof S., Geringer-Sameth A., Trotta R., 2020b, J. Cosmology Astropart. Phys., 2020, 012
Iacobelli M., et al., 2013, A&A, 558, A72
Intema H. T., Jagannathan P., Mooley K. P., Frail D. A., 2017, A&A, 598, A78
Jeltema T. E., Profumo S., 2008, ApJ, 686, 1045
Kar A., Mitra S., Mukhopadhyay B., Choudhury T. R., Tingay S., 2019, Phys. Rev. D, 100, 043002
Kar A., Mitra S., Mukhopadhyay B., Choudhury T. R., 2020, Phys. Rev. D, 101, 023015
Koposov S. E., Belokurov V., Torrealba G., Evans N. W., 2015, ApJ, 805, 130
Laevens B. P. M., et al., 2015, ApJ, 813, 44
Martin N. F., et al., 2015, ApJ, 804, L5
Martínez-Vázquez C. E., et al., 2019, MNRAS, 490, 2183
McConnachie A. W., 2012, AJ, 144, 4
McDaniel A., Jeltema T., Profumo S., Storm E., 2017, J. Cosmology Astropart. Phys., 2017, 027
Miville-Deschênes M. A., Duc P. A., Marleau F., Cuillandre J. C., Didelon P., Gwyn S., Karabal E., 2016, A&A, 593, A4
Natarajan A., Peterson J. B., Voytek T. C., Spekkens K., Mason B., Aguirre J., Willman B., 2013, Phys. Rev. D, 88, 083535
Natarajan A., Aguirre J. E., Spekkens K., Mason B. S., 2015, arXiv e-prints, p. arXiv:1507.03589
Navarro J. F., Frenk C. S., White S. D. M., 1996, ApJ, 462, 563
Profumo S., Ullio P., 2010, arXiv e-prints, p. arXiv:1001.4086
Regis M., Richter L., Colafrancesco S., Profumo S., de Blok W. J. G., Massardi M., 2015, MNRAS, 448, 3747
Rubin V. C., Ford W. K. J., Thonnard N., 1980, ApJ, 238, 471
Sparke L., Gallagher J., 2016, Galaxies in the Universe
Spekkens K., Mason B. S., Aguirre J. E., Nhan B., 2013, ApJ, 773, 61
Steigman G., Dasgupta B., Beacom J. F., 2012, Phys. Rev. D, 86
Storm E., Jeltema T. E., Spletstosser M., Profumo S., 2017, ApJ, 839, 33
Strigari L. E., 2018, Reports on Progress in Physics, 81, 056901
Strigari L. E., Bullock J. S., Kaplinghat M., Simon J. D., Geha M., Willman B., Walker M. G., 2008a, Nature, 454, 1096
Strigari L. E., Kousshiappas S. M., Bullock J. S., Kaplinghat M., Simon J. D., Geha M., Willman B., 2008b, ApJ, 678, 614
Vollmann M., Heesen V., W. Shinnwell T., Hardcastle M. J., Brüggen M., Sigl G., J. A. Röttgering H., 2020, MNRAS, 496, 2663
Walker M. G., Combt C., Hinton J. A., Maurin D., Wilkinson M. I., 2011, ApJ, 733, L46

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