Towards a Large-Area Freestanding Single-Crystal Ferroelectric BaTiO$_3$ Membrane

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Abstract: The fabrication and transfer of freestanding single-crystal ferroelectric membranes deserve intensive investigations as to their potential applications in flexible wearable devices, such as flexible data storage devices and varied sensors in E-skin configurations. In this report, we have shown a comprehensive study approach to the acquisition of a large-area freestanding single-crystal ferroelectric BaTiO$_3$ by the Sr$_3$Al$_2$O$_6$ scarification layer method. By controlling the thickness of the BaTiO$_3$ and Sr$_3$Al$_2$O$_6$, the exposed area of the Sr$_3$Al$_2$O$_6$ interlayer, and the utilization of an additional electrode La$_2$/3Sr$_1$/3MnO$_3$ layer, the crack density on the freestanding BaTiO$_3$ can be dramatically decreased from 24.53% to almost none; then, a more than 700 $\times$ 530 $\mu$m$^2$ area high-quality freestanding BaTiO$_3$ membrane can be achieved. Our results offer a clear and repeatable technology routine for the acquisition of a flexible large-area ferroelectric membrane, which should be instructive to other transition metal oxides as well. Our study can confidently boost flexible device fabrication based on single-crystal transition metal oxides.

Keywords: crack density; ferroelectrics; freestanding; single crystal

1. Introduction

Flexible single-crystal oxide membranes have attracted tremendous investigations, both experimentally and theoretically, due to their potential applications in wearable devices as well as for aiding our fundamental understanding of flexible electronics [1–3]. Different from the conventional metal [4,5] and organic materials [6,7], which offer a convenient fabrication of flexible membranes, the achievement of flexible transition metal oxides seems a tough task owing to that they always exhibit the nature of rigidity with poor fracture toughness, although transition metal oxides provide the unique physics properties, such as ferroelectricity [8], colossal magnetoresistance [9], and superconductivity [10], etc., benefiting to the multiple functionalities of future flexible wearable devices.

Barium titanate, BaTiO$_3$ (BTO), one of the most significant lead-free ferroelectrics [11,12], can be integrated in ultrathin all-oxide devices with high quality, such as the ferroelectric tunnel junction [13–15]. Its spontaneous polarization enables us to control the electrostatic state of a device easily by external electric voltage [16,17]. However, it is well known that the pronounced ferroelectricity needs a long-range lattice ordering [18]; thus, the fabrication of a large-area BTO single-crystal flexible membrane without cracks and a non-damage transfer process are definitely crucial.
Aiming for a flexible ferroelectric membrane, recently the ferroelectric BTO-based Van der Waals heterostructure [19] and the scarification layer method [13,20] have been developed rapidly. Although the flexible BTO can be achieved via depositing it on a mica substrate, the Van der Waals heterostructure cannot give a freestanding BTO layer, which blocks the possibility of the transfer process to any desired substrate.

On the other hand, the scarification layer method enables us to get a freestanding ferroelectric layer by the water-solved Sr$_3$Al$_2$O$_6$ (SAO) interlayer [21–24]. It is found that the freestanding single-crystal manganite La$_{0.7}$Sr$_{0.3}$MnO$_3$ [21], superconductor YBa$_2$Cu$_3$O$_{7-x}$ [22], and multiferroic BiFeO$_3$ [23] can be lifted off successfully. However, a systematic study on the preparation of a large-area single-crystal membrane without the local crack has not been reported in detail yet. Here, we report on a systemic investigation on the achievement of a large-area without any noticeable cracks. A freestanding ferroelectric BTO film with dimensions larger than 700 × 530 µm$^2$ has been achieved by the scarification layer method.

2. Materials and Methods

The Sr$_3$Al$_2$O$_6$ (SAO) target was prepared by the conventional solid-state method using SrCO$_3$ (99.95 purity) and Al$_2$O$_3$ (99.99 purity) powders (Aladdin Industrial Corporation in China) as the raw materials. The mixed powder was ground by an agate mortar for 8 h and then calcined at 1150 ºC for 5 h. After regrinding for 5 h, the powders were pressed into a pallet with a diameter of 30 mm and a thickness of 3.0 mm. Finally, the pallet was sintered in an alumina crucible at 1250 ºC for 24 h in air.

The La$_{2/3}$Sr$_{1/3}$MnO$_3$ (LSMO) target was mixed by SrCO$_3$ (99.95 purity), La$_2$O$_3$ (99.999 purity), and MnO$_2$ (99.95 purity) powders (Aladdin Industrial Corporation in China), and prepared in the same preparation process. The BTO target was the commercial one from the Kurt J. Lesker Company in America.

These targets were used to fabricate the BTO/SAO/STO (001) and LSMO/BTO/SAO/STO (001) heterostructures through a pulsed laser deposition (PLD) system with a KrF excimer laser of 248 nm wavelength. The base pressure was below 3 × 10$^{-7}$ Torr. During the deposition, the energy of the laser beam was adjusted to be 4.4 and 6.7 J/cm$^2$ for the SAO and BTO, while the oxygen partial pressure was maintained at 5 × 10$^{-5}$ and 4 × 10$^{-2}$ Torr. The laser pulse frequency was 2 Hz, and the substrate temperature was held at 700 and 750 ºC for the SAO and BTO, respectively. The LSMO cover layer was grown at 750 ºC, using 6.7 J/cm$^2$ at 2 Hz in a 0.2 Torr O$_2$ atmosphere. The thickness of the membranes was determined by the oscillation intensity of the reflection high-energy electron diffraction (RHEED).

The PFM characterizations were performed using a Dual AC Resonance Tracking piezoresponse force microscope (MFP-3D, Asylum Research, Oxford Instruments, America). The morphology of the membranes was observed by an optical microscope (Leica DM2700M, Leica, Germany).

Approximately 0.5-mm-thick polydimethylsiloxane (PDMS) was spread on a clean silicon wafer to make a flat PDMS sheet. Next, the top surface of the as-grown heterostructure adhered onto the PDMS surface. For obtaining the freestanding BTO membrane, the PDMS/BTO/SAO/STO (001) sample was immersed into de-ionized water for hours to completely dissolve the soluble SAO layer, and the growth substrate to be removed. The freestanding LSMO/BTO heterostructure was obtained in the same manner.

3. Results and Discussion

3.1. PFM Phase Analysis and Freestanding Membrane Transfer Process

In Figure 1a, we have shown the piezoelectric force microscopy (PFM) image of the BTO on Nb-doped STO to demonstrate that our BTO has an electric field, a switchable ferroelectric nature. The PFM phase image presents the regions with clear contrast, corresponding to the downward and upward polarizations written by ±5 V. Thus, we carried out the sacrificial layer method on a BTO layer with the same growth conditions. As shown in Figure 1b, firstly the Sr$_3$Al$_2$O$_6$ sacrificial layer
was deposited onto the SrTiO$_3$ (001) single-crystal substrate. Secondly, the BTO layer was grown on the SAO layer. Next, the heterostructure was adhered to the PDMS support layer and transferred to deionized water at room temperature for hours. Then the SAO sacrificial layer was dissolved in deionized water and the freestanding BTO membrane was obtained. Finally, we characterized the crack condition of the obtained freestanding BTO membrane by optical microscopy.

Figure 1. (a) The out-of-plane PFM phase image of the BTO membrane grown on an Nb:STO (001) substrate. (b) A schematic of the freestanding membrane transfer process.

3.2. The Relationship between Crack Density and Thickness for BTO Membranes

Crack density ($\rho$) is the key parameter to estimate the quality of membranes [25,26]. $\rho$ is determined by the following method: we selected six representative regions from one micrograph to calculate the average crack density. Cracks could be identified from the membrane accurately by setting the micrograph brightness threshold with a code developed in Python. The number of pixel points in the selected region is recorded as the film area ($S_0$), and the number of cracks pixel points, corresponding to the selected region, is recorded as the crack area ($S_C$). The average density of the cracks ($\rho$) can be calculated as $S_C/S_0 \times 100\%$. Figure 2e shows the original image of one representative region in Figure 2a, which is enclosed by the red dotted line. The output image is correspondingly shown in Figure 2e. Figure 2a–d shows the surface morphology of the different thickness of the BTO films (8.33, 16.7, 33.3, and 66.7 nm) transferred by a fixed 12.5-nm-thick SAO. Obviously, with the increase in the BTO membrane thickness, the crack density decreases from 19.42% to 9.35% (Figure 2e). From the literature, we know the oxide undergoes a lattice strain release after the flexibility process; thus, this will cause a huge internal strain distribution difference [22]. According to previous studies, similar to the semiconductor and metallic epitaxial layers, ferroelectric oxides are known to relieve the strain as the film thickness is increased [27,28]. Therefore, a large strain gradient is formed in the thinner BTO membrane, resulting in the appearance of dense cracks [29]. Moreover, regular wrinkles can be observed between the cracks (Figure 2a), which are formed perpendicular to the cracks, indicating that the BTO membranes prepared by the PLD system are very uniform [30].

3.3. The Relationship between Crack Density and Thickness for SAO Sacrificial Layers

Mechanical flexibility is a key property for flexible memories, yet most oxide single crystals or ceramics are hard and brittle that can be break at >4% strain [3]; thus, it is a big challenge for the oxide ferroelectric films to be used in the emerging flexible electronic devices. The strain $S$ induced on the surface of a substrate by bending the substrate into a radius of $R$ is given by the simplified equation: $S = (t_L + t_S)/2R$, where $t_L$ is the thickness of the layer and $t_S$ is the thickness of the substrate [31]. It can be seen from the simplified equation that the thinner film has excellent mechanical flexibility. So preparing high-quality 8.33-nm-thick BTO membranes should be a purpose for further exploration. Figure 3a–c present the evolution of cracks in the 8.33-nm-thick BTO membranes, which separated from the different thickness of the SAO sacrificial layers. It is clear that $\rho$ decreases from 24.53% to almost none with decreasing of the SAO layer thickness (Figure 3d). The thinner SAO sacrificial layer makes
the dissolved procedure much slower [21], and the stress between the membrane and the substrate gradually disappears, maintaining the integrity of the BTO membrane. When the SAO sacrificial layer thickness decreases down to 6.25 nm, the dissolution time is up to 24 h, and then no cracks appear in the partial areas.

![Optical micrographs of the BTO membranes with different thickness.](image)

**Figure 2.** Optical micrographs of the BTO membranes with different thickness. (a) 8.33 nm; (b) 16.7 nm; (c) 33.3 nm; (d) 66.7 nm. (e) Original image of the representative region in Figure 2a, which is enclosed by the red dotted line. (f) The output image corresponding to Figure 2e. (g) Variation in the crack density for the BTO membranes.

### 3.4. Process Improvement for High-Quality Membranes

Figure 3a,e show the two samples with the same preparation process, but the transfer processes between them are slightly different. Despite the large aspect ratio (700 × 530 µm²), almost no cracks were observed on the freestanding BTO membrane across the entire surface as a result of the improved transfer process, as shown in Figure 3a. On the other hand, Figure 3e presents the optical morphology of the BTO membrane, which was taken out from the deionized water directly, and lots of irregular and wide cracks on the surface can be seen clearly. This phenomenon is likely to be caused by water surface tension, which tears the ultrathin membrane when it separated from the substrate. To avoid the influence of water surface tension, the whole structure, including the substrate, was smoothly transferred to ethanol for 5 s, and then heated at 40 °C for 1 min to evaporate the water and alcohol. By this method, a large-area high-quality freestanding BTO membrane can be achieved.
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Figure 3. Optical micrographs of the 8.33-nm-thick BTO membranes separated from the SAO sacrificial layers with different thickness: (a) 6.25 nm; (b) 12.5 nm; (c) 30 nm. (d) Crack density for the BTO membranes as a function of the SAO thickness. (e) The freestanding BTO membranes separated from the deionized water directly. (f) Optical micrograph of the freestanding BTO membrane after the cross-section of the BTO/SAO/STO (001) structure was ground with fine sandpapers; the inset shows the cross-section structure was scraped with a blade.

During the deposition process of the BTO, the SAO sacrificial layer was completely covered by the BTO membrane and could not come in contact with the deionized water. Thus, the BTO membrane could not be separated from the growth substrate after the BTO/SAO/STO (001) structure was soaked for a week. To solve this problem, we scraped the cross-section of the BTO/SAO/STO (001) structure with a blade, making sure the SAO sacrificial layer was exposed to deionized water, and then the freestanding BTO membrane could be obtained successfully. In the morphology of the transferred BTO membrane, as shown in inset Figure 3f, a jagged edge structure appears in the BTO membrane scraped with a blade. The jagged edge structure increases the contact area between the SAO sacrificial layer and deionized water, which accelerates the dissolution rate, and the rapid stress change between the membrane and the substrate caused numerous cracks. To reduce the cracks in the edge area, we chose to use fine sandpapers (#1000) to grind the cross-section of the BTO/SAO/STO (001) structure slightly. Figure 3f shows the surface morphology of the treated structure, and the red dotted circle represents the edge of the membrane. The treated structure can be separated from the substrate after immersing...
in deionized water for up to 48 h, and then the edge of the membrane was very flat and no cracks appeared. It is important to note that all the heterostructure edges were ground by fine sandpaper, in order to obtain high-quality freestanding membranes.

3.5. The Relationship between Crack Density and the Thickness for LSMO Layers

Considering that the BTO membrane directly contacts the PDMS during the transfer process, it is difficult to obtain an intact surface due to non-uniform surface forces. An LSMO cover layer was grown on the BTO membrane to form an LSMO/BTO heterostructure, so the LSMO layer directly contacts the PDMS instead of the BTO during transfer. Additionally, the LSMO layer can be used as an electrode for electrical performance measurements [32].

Anja et al. reported the evolution of the in-plane lattice constant of the Pr$_{0.48}$Ca$_{0.52}$MnO$_3$ (PCMO) thin films ranging from 10 to 100 nm. For the 10-nm-thick sample, the \(a\) axes of film and substrate match perfectly, while the \(c\) axis is reduced compared to the bulk value. With increasing thickness, both the \(a\) and \(c\) axes of the PCMO film relax towards their bulk values, and the epitaxial strain may be relieved through the formation of cracks [33]. In the case of the LSMO (10 nm)/BTO (8.33 nm) heterostructure, the flat surface with cracks is clearly observed in Figure 4a. On the other hand, drastic change in the surface morphology above the LSMO (20 nm)/BTO (8.33 nm) and LSMO (30 nm)/BTO (8.33 nm) heterostructures were found, as shown in Figure 4b,c. The crack density increased systematically with increasing the LSMO layer thickness, as shown in Figure 4d. When the LSMO layer is grown epitaxially on the BTO membrane, in-plane tensile strain exists in the LSMO layer, caused by the lattice mismatch between the LSMO layer (\(~3.85\) Å) and the SAO sacrificial layer (\(~4.04\) Å). With increasing thickness of the LSMO layer, the lattice constant of the LSMO becomes smaller, leading to an increase in the epitaxial strain in the heterostructure. Then the epitaxial strain is clearly released by the formation of cracks.

![Figure 4](image-url)
4. Conclusions

To conclude, we systematically summarized the influence of the thickness of the SAO sacrificial layer and the BTO membrane on the crack density. By improving the transfer process, the BTO membrane with an area $>700 \times 530 \, \mu\text{m}^2$ with no cracks can be obtained from the BTO (8.33 nm)/SAO (6.25 nm)/STO (001) substrate structure. Then, we improved the positive effect of the LSMO cover layer with the electrode function on crack elimination. After being separated from the substrate, a high-quality freestanding LSMO (10 nm)/BTO (8.33 nm) heterojunction can be obtained. On this basis, an unprecedented very large strain gradient can be generated by altering the radius of the freestanding single-crystal BTO membrane, the flexoelectric effects of which are yet to be explored.

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