The Monitor project: Rotation of low-mass stars in the open cluster NGC 2516

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Accepted .... Received ...; in original form ...

\textbf{ABSTRACT}

We report on the results of an \textit{i}-band time-series photometric survey of NGC 2516 using the CTIO 4m Blanco telescope and 8k Mosaic-II detector, achieving better than 1\% photometric precision per data point over 15 $\lesssim i \lesssim 19$. Candidate cluster members were selected from a $V$ vs $V − I$ colour magnitude diagram over 16 $< V < 26$ (covering masses from 0.7 $M_\odot$ down to below the brown dwarf limit), finding 1685 candidates, of which we expect $\sim 1000$ to be real cluster members, taking into account contamination from the field (which is most severe at the extremes of our mass range). Searching for periodic variations in these gave 362 detections over the mass range 0.15 $\lesssim M/M_\odot \lesssim 0.7$. The rotation period distributions were found to show a remarkable morphology as a function of mass, with the fastest rotators bounded by $P > 0.25$ days, and the slowest rotators for $M < 0.5 M_\odot$ bounded by a line of $P \propto M^{−3}$, with those for $M \gtrsim 0.5 M_\odot$ following a flatter relation closer to $P \sim$ constant. Models of the rotational evolution were investigated, finding that the evolution of the fastest rotators was well-reproduced by a conventional solid body model with a mass-dependent saturation velocity, whereas core-envelope decoupling was needed to reproduce the evolution of the slowest rotators. None of our models were able to simultaneously reproduce the behaviour of both populations.

\textbf{Key words:} open clusters and associations: individual: NGC 2516 – techniques: photometric – stars: rotation – surveys.

1 INTRODUCTION

NGC 2516 is a well-studied nearby intermediate-age open cluster ($\sim 150$ Myr, \textcite{JeffriesThurstonHambly2001}, at a distance modulus $(M − m)_0 = 7.93 ± 0.14$ \textcite{Terndrupetal2002}). The canonical reddening along the line of sight to the cluster is $E(B−V) = 0.12$, implying a photometrically derived metallicity of $[\text{Fe/H}] = −0.05 ± 0.14$ \textcite{Terndrupetal2002}. The same authors derive a spectroscopic metallicity from two stars of $[\text{Fe/H}] = 0.01 ± 0.03$, consistent within the errors, and implying a slightly larger distance modulus $(M − m)_0 = 8.05 ± 0.11$. We have adopted the smaller distance modulus $(M − m)_0 = 7.93 ± 0.14$ and photometric metallicity for the remainder of this work, but any differences induced in the results by the uncertainty in distance modulus are nevertheless small.

NGC 2516 has often been referred to as the ‘Southern Pleiades’ owing to its similarity both in angular extent and age, where we adopt an age of 100 Myr \textcite{Meynetetal1994} for the Pleiades, using the classical main sequence turnoff ages throughout this work for consistency with the estimate for NGC 2516. The Pleiades metallicity is very similar, at $[\text{Fe/H}] = −0.034 ± 0.024$ \textcite{BoesgaardFriel1990}, Clusters in the age range between $\alpha$ Persei ($\sim 50$ Myr, e.g. \textcite{BasriMartín1999}) and the Hyades ($\sim 625$ Myr, \textcite{Perrymanetal1998}) are important for constraining stellar evolution models. Figure 1 shows a plot of the age at which a solar metallicity star reaches the zero age main sequence (ZAMS) as a function of stellar mass, indicating that solar mass stars reach the ZAMS at $\sim 40$ Myr, and $\sim 0.4−0.5 \, M_\odot$ stars reach the ZAMS at the age of NGC 2516. It is therefore highly useful in this regard owing to both its age and relative proximity, where we can study solar mass stars after evolving for a short time on the main sequence, and lower mass stars as they finish pre main sequence evolution. The similarity in age to the Pleiades (modulo the uncertainty in this parameter) means that comparisons of these clusters
could be used to study the dependence of stellar parameters on environment.

NGC 2516 is very well-studied in the literature. The most relevant existing work includes membership surveys (Jeffries et al. 2001, Sung et al. 2002), characterisation of the mass function from solar mass (Jeffries et al. 2001), down to the brown dwarf regime (Moraux et al. 2001), a survey for radial velocities and binarity at the bright end of the cluster sequence (González & Lapasset 2000), and studies of rotation using $v\sin{i}$ covering stars down to G spectral types (Terndrup et al. 2002 and Jeffries, James & Thurston 1998). A number of X-ray surveys, including monitoring for variability, have also been carried out (e.g. Wolk et al. 2004, Ramsay, Harra & Kay 2003, Damiani et al. 2003, Sciotino et al. 2001). The most recent of which (Pilitteri et al. 2006) used a deep XMM-Newton observation to probe the low-mass members (down to $\sim$ M5) of the cluster. They found that NGC 2516 stars are less luminous in X-rays than the Pleiades members, and suggest that this may be attributed to slightly older age, or lower rotation rates.

1.1 Evolution of stellar angular momentum

For a discussion of the context of this work, the reader is referred to our M34 publication in Irwin et al. (2006). The present survey probes a different open cluster of slightly younger age ($\sim$ 150 Myr for NGC 2516, compared to $\sim$ 200 Myr for M34). Due to the small distance modulus and our use of a larger telescope, the NGC 2516 survey probes lower masses, covering a range of $0.1 < M/M_\odot < 0.7$, compared to $0.25 < M/M_\odot < 1.0$ in M34, allowing the very low-mass stars to be examined in much greater detail. This will allow models of angular momentum evolution to be tested over a wider range of stellar mass, in particular to determine whether models incorporating solid body rotation (e.g. Bouvier, Forestini & Allain 1997) are able to reproduce the observed low-mass angular momentum evolution. At the lowest masses, core-envelope decoupling should not be relevant, since all the stars will be fully-convective and thus rotate approximately as solid bodies, allowing us to constrain directly the angular momentum loss law without needing to consider the details of internal angular momentum transport. At the age of NGC 2516, stars with masses $M < 0.4 M_\odot$ should be fully-convective (Chabrier & Baraffe 1997).

1.2 The survey

We have undertaken a photometric survey in NGC 2516 using the CTIO 4m Blanco telescope and Mosaic-II imager. Our goals are two-fold: first, to study rotation periods for a sample of low-mass members, covering M spectral types, down to $\sim 0.1 M_\odot$, and second, to look for eclipsing binary systems containing low-mass stars, to obtain dynamical mass measurements in conjunction with radial velocities from follow-up spectroscopy. Such systems provide the most accurate determinations of fundamental stellar parameters (in particular, masses) for input to models of stellar evolution, which are poorly constrained in this age range. We defer discussion of our eclipsing binary candidates to a later paper once we have obtained suitable follow-up spectroscopy.

These observations are part of a larger photometric monitoring survey of young open clusters over a range of ages and metallicities (the Monitor project; Hodgkin et al. 2006 and Aigrain et al. in press).

The remainder of the paper is structured as follows: the observations and data reduction are described in §3 and the colour magnitude diagram (CMD) of the cluster and candidate membership selection are presented in §3. The method we use for obtaining photometric periods is summarised in §4 (see Irwin et al. 2006 for a more detailed discussion), and our results are summarised in §5. We discuss the implications of these results in §6, and our conclusions are summarised in §7.

In several of the following sections, we use mass and radius estimates for the cluster members. We note here that these were derived from the 150 Myr NextGen models, using the $I$-band magnitudes, rather than $V - I$ colour or $V$ magnitude, for reasons discussed in §3.

2 OBSERVATIONS AND DATA REDUCTION

Photometric monitoring observations were obtained using the 4m CTIO Blanco telescope, with the Mosaic-II imager, during two four-night observing runs, separated by $\sim$ 1 week, in 2006 February-March. This instrument provides a field of view of $36' \times 36'$ (0.37 sq.deg), using a mosaic of eight 2k x 4k pixel CCDs, at a scale of $0.27''$/pix. NGC 2516 was observed for $\sim$ 8 hours per night.

In order to maximise the number of cluster members covered by our survey, and given the large angular extent of NGC 2516, we used three fields, with a single 75 s $i$-band exposure in each, observed by cycling around all three fields, to give a cadence of $\sim$ 9 minutes, covering $\sim$ 1 sq.deg of the cluster (illustrated in Figure 2). Our fields were chosen to be outside the central few arcmin of the cluster to avoid contamination of the images from a number of very bright ($V \sim 5 - 8$) stars close to the cluster centre.

The observing conditions were superb, with exceptional seeing (< 0.8'' on a few nights) and $\sim$ 6 photometric nights.
We also obtained a number of longer $V$-band exposures in photometric conditions ($3 \times 300s$ in each field) to generate a colour magnitude diagram (CMD). Our observations are sufficient to give 1% or better photometric precision per data point from saturation at $i \sim 15$ down to $i \sim 19$ (see Figure 3), covering early to mid M spectral types at the age and distance of NGC 2516.

For a full description of our data reduction steps, the reader is referred to Irwin et al. (in press). Briefly, we used the pipeline for the INT wide-field survey (Irwin & Lewis 2001) for 2-D instrumental signature removal (crosstalk correction, bias correction, flatfielding) and astrometric and photometric calibration. We then generated the master catalogue for each filter by stacking 20 of the frames taken in the best conditions (seeing, sky brightness and transparency) and running the source detection software on the stacked image. The resulting source positions were used to perform aperture photometry on all of the time-series images. We achieved a per data point photometric precision of $\sim 2 - 4$ mmag for the brightest objects, with RMS scatter $< 1\%$ for $i \lesssim 19$ (see Figure 3).

Our source detection software flags as likely blends any objects detected as having overlapping isophotes. This information is used, in conjunction with a morphological image classification flag also generated by the pipeline software (Irwin & Lewis 2001) to allow us to identify non-stellar or blended objects in the time-series photometry.

Photometric calibration of our data was carried out using regular observations of Landolt (1992) equatorial standard star fields in the usual way.

Lightcurves were extracted from the data for $\sim 100\,000$ objects, 63,000 of which had stellar morphological classifications, using our standard aperture photometry techniques, described in Irwin et al. (in press). We fit a 2-D quadratic polynomial to the residuals in each frame (measured for each object as the difference between its magnitude on the frame in question and the median calculated across all frames) as a function of position, for each of the 8 CCDs separately. Subsequent removal of this function accounted for effects such as varying differential atmospheric extinction across each frame. Over a single CCD, the spatially-varying part of the correction remains small, typically $\sim 0.02$ mag peak-to-peak. The reasons for using this technique are discussed in more detail in Irwin et al. (in press).

For the production of deep CMDs, we stacked 20 $i$-band observations, taken in good seeing and photometric conditions. The limiting magnitudes, measured as the approximate magnitude at which our catalogues are 50% complete (see 3.2) on these images were $V \simeq 24.3$ and $i \simeq 22.7$.

## 3 SELECTION OF CANDIDATE LOW-MASS MEMBERS

Catalogues of photometrically-selected candidate members were available from Jeffries et al. (2001) for solar mass down to $\sim 0.2\,M_\odot$ and for $\sim 0.2 - 0.05\,M_\odot$ from Moraux et al. (2003), but we elected to perform a new photometric selection using $V$ versus $V - I$ CMDs from our data, to match exactly the field of view and magnitude range of our time-series photometry. Unfortunately, since we have avoided the very centre of the cluster in our field selection to reduce the effect of saturated bright stars on our CCD frames, the overlap in sky coverage between the present survey and many of the previous ones (e.g. Jeffries et al. 2001 and Pillitteri et al. 2004) is relatively poor.

### 3.1 The $V$ versus $V - I$ CMD

Our CMD of NGC 2516 is shown in Figure 4. The $V$ and $i$ measurements were converted to the standard Johnson-Cousins photometric system using colour equations derived from our standard star observations:

$$V - I = (V_{\text{ccd}} - i_{\text{ccd}}) / 0.899$$

(1)
Figure 4. $V$ versus $V-I$ CMD of NGC 2516 from stacked images, for all objects with stellar morphological classification. The cluster main sequence is clearly visible on the right-hand side of the diagram. The boundaries of the region to select photometric candidate members are shown by the dashed lines (all objects between the dashed lines were selected). The reddening vector for $A_V = 1.0$ is shown at the right-hand side of the diagram. The mass scale is from the 150 Myr NextGen models (Baraffe et al. 1998) for $M > 0.1 \, M_\odot$, and the 120 Myr DUSTY models (Chabrier et al. 2000) for $M < 0.1 \, M_\odot$, using our empirical isochrone to convert the $V$ magnitudes to $I$ magnitudes, and subsequently obtaining the masses from these, due to known problems with the $V$ magnitudes from the models (see §3.1). The error bars at the left-hand side of the plot indicate the typical photometric error for an object on the cluster sequence.

\begin{align*}
V &= V_{\text{ccd}} + 0.005 \, (V-I) \\
I &= i_{\text{ccd}} - 0.096 \, (V-I) \quad (2) \quad (3)
\end{align*}

Candidate cluster members were selected by defining an empirical main sequence ‘by eye’ to follow the clearly-visible cluster single-star sequence. The cuts were defined by moving this line along a vector perpendicular to the cluster sequence, by amounts $k-\sigma(V-I)$ and $k+\sigma(V-I)$ as measured along this vector, where $\sigma(V-I)$ is the photometric error in the $V-I$ colour. The values of $k$ used were $-0.15$ mag for the lower line and $0.5$ mag for the upper line on the diagram, making the brighter region wider to avoid rejecting binary and multiple systems, which are overluminous for their colour compared to single stars. 1685 candidate photometric members were selected, over the full $V$ magnitude range from $V = 15.5$ to 26, but the well-defined main sequence appears to terminate at the hydrogen burning mass limit of $M \sim 0.072 \, M_\odot$, or $V \sim 24$, with a few candidate brown dwarfs found below this limit, but with high field contamination.

We also considered using the model isochrones of Baraffe et al. (1998) and Chabrier et al. (2000) for selecting candidate members. The NextGen model isochrones were found to be unsuitable due to the known discrepancy between these models and observations in the $V-I$ colour for $T_{\text{eff}} < 3700$ K (corresponding here to $V-I > 2$). This was examined in more detail by Baraffe et al. (1998), and is due to a missing source of opacity at these temperatures, leading to overestimation of the $V$-band flux. Consequently, when we have used the NextGen isochrones to determine model masses and radii for our objects, the $I$-band absolute magnitudes were used to perform the relevant look-up, since these are less susceptible to the missing source of opacity, and hence give more robust estimates.

3.2 Completeness

The completeness of our source detection was estimated by inserting simulated stars at random $x, y$ positions into our images, drawing the stellar magnitudes from a uniform distribution. Figure 5 shows the resulting plot of completeness as a function of $V$-band magnitude. The completeness for objects on the cluster sequence is $> 90\%$ down to the BD limit ($V \sim 24$). We suspect that the gradual drop in completeness toward fainter magnitudes in Figure 5 results from a variable background in our CCD images caused by halos and scattered light from the many bright stars in the cluster field, impeding detection of faint sources in certain regions of the frame.

![Figure 5. Completeness in our source detection, measured as the fraction of simulated objects which were detected in each magnitude bin. The diagram is plotted in the Johnson $V$ system assuming objects to lie on the empirically-derived cluster main sequence track of §3.1 and Figure 4. The diagram has been terminated at $V = 26$ since we have not continued the selection of cluster members past this magnitude due to termination of the apparent main sequence in the CMD of Figure 4.](image-url)
apparently very high contamination in the more accurate estimate. We note in particular that the V contamination level of ∼39%. Figure 6 shows the contamination as a function of V magnitude. We note that this figure is somewhat uncertain due to the need to use Galactic models, Follow-up data (spectroscopy) will be required to make a more accurate estimate. We note in particular that the apparently very high contamination in the V = 16 – 17 bin, and possibly also the V = 25 – 26 bin, is probably the result of the model poorly-fitting the observations, causing the contamination level to be overestimated.

3.3 Contamination

In order to estimate the level of contamination in our catalogue, we used the Besançon Galactic models (Robin et al. 2004) to generate a simulated catalogue of objects passing our selection criteria at the Galactic coordinates of NGC 2516 (l = 273.8°, b = −15.9°), covering the total FoV of ∼1.1 sq.deg (including gaps between detectors). We selected all objects over the apparent magnitude range 14 < V < 26, giving 105,000 stars. The same selection process as above for the cluster members was then applied to find the contaminant objects. A total of 651 simulated objects passed these membership selection criteria, giving an overall contamination level of ∼39%. Figure 6 shows the contamination as a function of V magnitude. We note that this figure is somewhat uncertain due to the need to use Galactic models. Follow-up data (spectroscopy) will be required to make a more accurate estimate. We note in particular that the apparently very high contamination in the V = 16 – 17 bin, and possibly also the V = 25 – 26 bin, is probably the result of the model poorly-fitting the observations, causing the contamination level to be overestimated.

3.4 Binary fraction

Since the cluster binary sequence is so clearly visible in the CMD of Figure 4, we have computed a simple photometric lower limit for the binary fraction in the cluster as a function of mass, using the empirical isochrone to select stars with luminosities lying within a band of height 2.5 log 0.2 z 0.75 mag centred on the single star cluster sequence, and the binary sequence (obtained by shifting the cluster sequence by this amount to greater luminosities), illustrated in Figure 4. This technique suffers from several sources of systematic error, including: (a) since the single star sequence is closer to the maximum of the distribution of field stars in the CMD, the single star counts are increased to a greater degree than the binary counts by field contamination, (b) binaries with mass ratios significantly different from 1 lie closer to the single star sequence, and therefore tend not to be selected as binaries, and (c) at the faint end of the CMD the binaries are brighter, and hence more readily detected than single stars of the same colour.

The binary fraction is shown as a function of mass in Figure 8. A total of 357 candidate binaries and 1065 candidate single stars were selected, giving an overall binary fraction of 33.5 ± 2.1% (using Poisson errors).

We have been unable to use the more traditional I – K CMD approach (e.g. Pinfield et al. 2003) to determining limits on the binary fraction due to the lack of suitable near-IR data. 2MASS provides K-band photometry, but the resulting I – K CMD did not show a clearly-visible binary sequence due to the large scatter caused by the photometric errors at the faint end of 2MASS.

At this point, it is prudent to examine the sensitivity of our selection to the mass ratio q of the binaries. To do this, we have simulated binaries over a range of q from 0 to 1.0, using the PMS models to compute the total I-band luminosity of the binary, and our empirical isochrone to convert the individual I-band magnitudes of the primary and secondary to V-band, and hence place the objects on the V – I CMD. Our selection was then applied to determine the minimum mass ratio q for the detected binaries, defined as q = M_2/M_1 (where M_1 and M_2 are the primary and
secondary masses, respectively). In general we find that our selection is sensitive to smaller mass ratios at lower masses, which could explain the form of the binary fraction as a function of mass, given the small number statistics (and hence large Poisson errors in Figure 5) and better sensitivity to small q with decreasing mass (leading presumably to more detections).

Photometric selection of binaries remains, to our knowledge, relatively untested, without detailed evaluation of the sensitivity. Therefore, a more detailed and reliable study of the fraction in NGC 2516 requires follow-up spectroscopy.

4 PERIOD DETECTION

4.1 Method

The method we use for detection of periodic variables is described in detail in Irwin et al. (2006), and we provide only a brief summary here. The method uses least-squares fitting of sine curves to the time series m(t) (in magnitudes) for all candidate cluster members, using the form:

\[ m(t) = m_{dc} + \alpha \sin(\omega t + \phi) \]  

where \( m_{dc} \), \( \alpha \) (the amplitude) and \( \phi \) (the phase) are free parameters at each value of \( \omega \) over an equally-spaced grid of frequencies, corresponding to periods from 0.005 – 50 days for the present data-set.

Periodic variable lightcurves were selected by evaluating the change in reduced \( \chi^2 \):

\[ \Delta \chi^2 = \chi^2_{\omega, smooth} - \chi^2_{\omega} > 0.4 \]  

where \( \chi^2_{\omega, smooth} \) is the reduced \( \chi^2 \) of the original lightcurve with respect to a constant model, and \( \chi^2_{\omega} \) is the reduced \( \chi^2 \) of the lightcurve with the smoothed, phase-folded version subtracted. This threshold was used for the M34 data and appears to work well here too, carefully checked by examining all the lightcurves for two of the detectors, chosen randomly. A total of 1011 objects were selected by this automated part of the procedure.

The selected lightcurves were examined by eye, to define the final sample of periodic variables. A total of 362 lightcurves were selected, with the remainder appearing non-variable or too ambiguous to be included.

4.2 Simulations

Monte Carlo simulations were performed following the method detailed in Irwin et al. (2006), injecting simulated signals of 2% amplitude and periods chosen following a uniform distribution on log10 period from 0.1 to 20 days, into lightcurves covering a uniform distribution in mass, from 0.7 to 0.1 M⊙. A total of 2271 objects were simulated.

The results of the simulations are shown in Figure 10 as greyscale diagrams of completeness, reliability and contamination as a function of period and stellar mass. Broadly, our period detections are close to 100% complete down to 0.2 M⊙, with remarkably little period dependence. The slight incompleteness (approximately 63% completeness for
0.6 < M/M⊙ < 0.7) seen in the highest mass bin is a result of saturation. Figure 11 shows a comparison of the detected periods with real periods for our simulated objects, indicating remarkably high reliability, especially compared to the earlier M34 data-set (Irwin et al. 2006), resulting from better sampling.

4.3 Detection rate and reliability

The locations of our detected periodic variable candidate cluster members on a V versus V − I CMD of NGC 2516 are shown in Figure 12. The diagram indicates that the majority of the detections lie on the single-star cluster main sequence, as would be expected for rotation in cluster stars as opposed to, say, eclipsing binaries. The measured photometric binary fraction (see §3.4) for the periodic variable stars is 26.3 ± 3.5% (using Poisson errors). This value is slightly lower than the value for all cluster members from §3.4 but only at the 1.8σ level. Given the systematic uncertainties in the binary fractions (which are not accounted for by the Poisson counting errors), this is probably not a significant result.

Figure 13 shows the fraction of cluster members with detected periods as a function of V magnitude. The decaying parts of the histogram at the bright and faint ends may be caused by the increased field contamination here (see Figure 9), since we expect field objects on average show less rotational modulation than cluster objects, and/or incompleteness effects resulting from saturation for V ≤ 17, and for V ≥ 21, the gradual increase in the minimum amplitude of variations we can detect (corresponding to the reduction in sensitivity moving to fainter stars, see Figure 3).

In the M34 survey of Irwin et al. (2006), we commented...
on a possible increase in the fraction of photometric variables from $K$ to $M$ spectral types, subject to a large uncertainty due to small number statistics. Since the mass range covered by the present sample is different, direct comparison is difficult, and there is no clear evidence for such a trend in NGC 2516. We further note that the decline observed in M34 at faint magnitudes is probably indeed due to incompleteness as stated by Irwin et al. (2006), since a similar trend is also seen in the NGC 2516 data-set, displaced accordingly for the differences in sensitivity and distance modulus.

We note that lower field contamination (as evaluated in §3.3) is expected in the rotation sample than in the full candidate membership sample. Typical field population ages for the young disc of 3 Gyr (Mayor 1974, Meusinger, Stecklum & Reimann 1991) imply slower rotation rates by factors of a few than cluster members, reduced activity, implying smaller asymmetric components of the spot coverage and hence lower photometric amplitudes (which probably render many of them undetectable).

The properties of all our rotation candidates are listed in Table 1.

4.4 Non-periodic objects

The population of objects rejected by the period detection procedure described in §4 was examined, finding that the most variable population of these lightcurves (which might correspond to non-periodic or semi-periodic variability) was contaminated by a small number of lightcurves ($\sim 50$) exhibiting various uncorrected systematic effects, mostly seeing-correlated variations due to image blending. It is therefore difficult to quantify the level of non-periodic or semi-periodic variability in NGC 2516 from our data. Qualitatively however, there appear to be very few of these variables, and examining the lightcurves indicated only $\sim 10$ obvious cases, some of which resembled eclipses (either planetary transits or eclipsing binaries), and will be the subject of a later Monitor project paper.

5 RESULTS

5.1 NGC 2516 rotation periods

Plots of period as a function of $V - I$ colour and mass for the objects photometrically selected as possible cluster members are shown in Figure 15. These diagrams show a striking correlation between stellar mass (or spectral type) and the longest rotation period seen at that mass, with a clear lack of slow rotators at very low masses. This trend is also followed by the majority of the rotators, with only a tail of faster rotators to $\sim 0.25$ day periods. Furthermore, very few objects were found rotating faster than this, implying a hard lower limit to the observed rotation periods at 0.25 days.
Table 1. Properties of our 362 rotation candidates. The period \( P \) in days, \( i \)-band amplitude \( \alpha_i \) (units of magnitudes, in the instrumental bandpass), interpolated mass and radius (from the models of Baraffe et al. 1998, derived using the \( I \) magnitudes) are given (where available). Our identifiers are formed using a simple scheme of the cluster name, field number, CCD number and a running count of stars in each CCD, concatenated with dashes. The full table is available in the electronic edition.

| Identifier | RA \( \text{J2000} \) | Dec \( \text{J2000} \) | \( V \) mag | \( I \) mag | \( P \) days | \( \alpha_i \) mag | \( M \) \( M_\odot \) | \( R \) \( R_\odot \) |
|------------|----------------|-----------------|----------|----------|---------|-----|----|----|
| N2516-1-1-351 | 07 56 28.22 | -61 27 46.6 | 18.99 | 16.35 | 2.318 | 0.016 | 0.44 | 0.41 |
| N2516-1-1-784 | 07 56 43.99 | -61 30 51.5 | 21.25 | 18.05 | 0.649 | 0.013 | 0.20 | 0.24 |
| N2516-1-1-881 | 07 56 47.57 | -61 34 37.9 | 17.80 | 15.54 | 7.677 | 0.010 | 0.55 | 0.51 |
| N2516-1-1-958 | 07 56 49.99 | -61 32 19.9 | 18.48 | 15.99 | 6.291 | 0.015 | 0.49 | 0.45 |
| N2516-1-1-1470 | 07 57 08.92 | -61 29 18.6 | 17.67 | 15.49 | 8.803 | 0.016 | 0.56 | 0.52 |

Figure 14. Plots of rotation period as a function of dereddened \( V - I \) colour (top), and mass (bottom) for NGC 2516, deriving the masses using the 150 Myr NextGen mass-magnitude relations of Baraffe et al. (1998) and our measured \( I \)-band magnitudes. In the lower diagram, the greyscales show the completeness for 0.02 mag periodic variations from our simulations, and X-ray sources from Pillitteri et al. (2006) are overlaid with open circles.

Could the apparent morphology in Figure 14 be explained by sample biases? The simulations of Figure 12 suggest that this is unlikely, since we are sensitive to shorter periods than the 0.2 – 0.3 day ‘limit’, and the slight bias toward detection of shorter periods at low mass is not sufficient to explain the observations for the slow rotators. Furthermore, Figure 15 indicates that the lack of sensitivity to low amplitudes at low masses does not appear to introduce any systematic changes in the detected periods.

Figures 14 and 15 show an apparent lack of objects with masses \( 0.2 < M / M_\odot < 0.4 \) and rotation periods \( \gtrsim 2 \) days, a region of the diagram where our survey is sensitive down to amplitudes of 0.01 mag (see also Figure 12). There is also an apparent lack of large-amplitude objects in this region of the diagram, although this is not statistically significant (applying a Kolmogorov-Smirnov test between the two mass bins indicated a probability of 0.25 that the distributions were drawn from the same parent population).

5.1.1 Period distributions

In order to quantify the morphology of Figure 14 we have used histograms of the rotation period distributions in two broad mass bins, \( 0.4 < M / M_\odot < 0.7 \) and \( M < 0.4 \) \( M_\odot \), shown in Figure 16. We have attempted to correct the distributions for the effects of incompleteness and (un)reliability.
using the simulations described in [12] following the method used in [Irwin et al. 2006]. The results of doing this are shown in the solid histograms in Figure [15] and the raw period distributions in the dashed histograms.

The period distributions in the two mass bins of Figure [16] show clear differences, with the low-mass stars ($M < 0.4 M_\odot$) showing a strongly peaked rotational period distribution, with a maximum at $\approx 0.6 - 0.7$ days, whereas the higher-mass stars (0.4 $M_\odot < M < 0.7$) show a broader distribution. We applied a two-sided Kolmogorov-Smirnov test to the corrected distributions to confirm the statistical significance of this result, finding a probability of $4 \times 10^{-20}$ that the distributions were drawn from the same parent population.

The implication of this result is that the observed morphology in Figure [13] and in particular the increase of the longest observed rotation period as a function of increasing mass, a trend followed also by the bulk of the rotators, is real and statistically significant.

5.1.2 Low-mass slow rotators

A group of $\approx 4$ outliers are visible e.g. in the upper panel of Figure [14] as unusually slow rotators at low mass ($(V-I) \gtrsim 2.5$). These objects also give rise to the apparent ‘trend’ seen in Figure [15] of smaller amplitudes for periods $P \gtrsim 2$ days, for the lower mass bin ($0.2 < M/M_\odot \lesssim 0.4$).

Careful examination of the lightcurves indicates that these objects are all convincing detections, and lie on, or close to, the cluster sequence. Obtaining optical spectroscopy for these objects would appear to be warranted, to constrain their membership of the cluster, and determine spectral types, to evaluate their reddening.

5.1.3 Rapid rotators

We have examined the periods of our fastest-rotating stars, to check if they are rotating close to their break-up velocity. The critical period $P_{\text{crit}}$ for break-up is given approximately by:

$$P_{\text{crit}} = 0.116 \text{ days} \times \left( \frac{R/R_\odot}{M/M_\odot} \right)^{3/2} \left( \frac{M/M_\odot}{M_\odot} \right)^{1/2}$$

where $R$ and $M$ are the stellar radius and mass respectively (e.g. Herbst et al. 2002). Using the NextGen models of Baraffe et al. (1998), the object rotating closest to breakup is N2516-2-8-624, with $P_{\text{crit}}/P = 0.42$. However, the majority of our objects are rotating at much lower fractions of their break-up velocity.

Figure [15] indicates that all but three of our fastest rotators have $P > 0.2$ days. The outliers are N2516-1-4-3373 ($P = 0.148$ days), N2516-2-8-566 ($P = 0.146$ days) and N2516-2-8-624 ($P = 0.087$ days). Two of these objects, N2516-1-4-3373 and N2516-2-8-624, clearly lie on the binary sequence in Figure [13] and N2516-2-8-566 may also lie on the binary sequence, so we suspect that these stars might be tidally locked binaries. They are therefore good candidates for spectroscopic follow-up.

We note that there are three outliers visible in Figure [14] with $(V-I) < 1.3$, and periods close to 1 day. Similar objects were seen in our M34 study (Irwin et al. 2006). At these masses, field contamination in our survey is significant ($\approx 60\%$), so we suspect that they may be contaminating field objects, and possibly binaries (in M34, several of the corresponding objects were also detected in X-rays, it is difficult to say if this holds in NGC 2516 due to the incomplete overlap in spatial coverage with the X-ray catalogue of Pillitteri et al. 2006). Our survey is incomplete at these (high) masses due to saturation of the detectors, which varied between CCDs in the mosaic, giving rise to the lack of other objects detected in this range of $(V-I)$.

5.2 Comparison with other data-sets

5.2.1 Period versus mass diagram

Figure [17] shows a diagram of rotation period as a function of stellar mass for the ONC (1 $\pm 1$ Myr; Hillenbrand [1997]), NGC 2264 (2 $\pm 4$ Myr; Park et al. 2000), NGC 2362 ($\sim 5 \pm 1$ Myr; Moitinho et al. 2001, Balona & Laney 1999), the Pleiades ($\sim 100$ Myr; Meynet et al. 1993), NGC 2516 and M34 ($\sim 200$ Myr; Jones & Prosser 1996). Data sources for each cluster are indicated in the figure caption. From this Figure, it appears that the objects we observe in NGC 2516 are bounded by lines of $P$ constant (or a low power of $M$) for the fastest rotators, and $P \propto M^3$ for the slow rotators in the mass range $0.2 < M/M_\odot < 0.7$.

Furthermore, comparing the NGC 2516 and M34 results in Figure [17] indicates that the slowest rotators for $M > 0.6 M_\odot$ have $P$ constant as a function of mass, whereas for $M < 0.6 M_\odot$, the period increases as a function of mass. A similar trend is visible in the Pleiades $v\sin i$ data (noting that a number of the slowest rotators here only have $v\sin i$ lower limits, denoted by double-headed arrows).

The diagram clearly shows a gradual evolutionary sequence, from a relatively flat mass-dependence of the rotation periods in the ONC ($\sim 1$ Myr), to a sloping relation in NGC 2362 ($\sim 5$ Myr), and the emergence of the break between a flat distribution for $M \gtrsim 0.6 M_\odot$ and strongly sloping distribution at lower masses, for the Pleiades, NGC 2516 ($\sim 150$ Myr) and M34 ($\sim 200$ Myr). We suggest this apparent change in slope at $M \sim 0.6 M_\odot$ may correspond to a transition to convectively-dominated stellar interiors moving to lower masses (but see §5.2).

5.2.2 $v\sin i$ measurements

Terndrup et al. (2002) presented $v\sin i$ measurements for G and early-K dwarfs in NGC 2516. Dividing their sample into branches of fast and slow rotation for $(B-V)_0 > 0.6$ and counting objects with $v\sin i < 15$ km s$^{-1}$ as slow rotators, gave 7 fast rotators, with typical $v\sin i \sim 20 - 50$ km s$^{-1}$, and 17 slow rotators with $v\sin i \lesssim 10$ km s$^{-1}$, i.e. 30% are fast rotators. The threshold of $v\sin i = 15$ km s$^{-1}$ corresponds to $P = 2.2$ $\sin i$ days at $0.7 M_\odot$, or $(P) = 1.72$ days, using $(\sin i) = \pi/4$ (averaged over all inclinations $i$). Applying this threshold to the 0.5 $\pm 0.7 M_\odot$ bin of Figure [13] we counted 69 slow rotators, and 40 fast rotators, i.e. 37% fast rotators (and clearly from Figure [13] this fraction increases considerably for lower masses, to nearly 100% at $0.2 M_\odot$). Furthermore, for $(B-V)_0 < 0.6$ there are no clearly-visible fast rotators in Figure 5 of Terndrup et al. (2002). These results clearly indicate that the fraction of objects rotating
faster than the chosen threshold increases as a function of mass, lending support to the rotation period results we have presented.

5.2.3 Comparison to the field: main sequence spin-down
Comparing our results with the field survey of Delfosse et al. (1998) indicates that the spin-down timescale of M-dwarfs increases moving to later spectral types (or lower masses). The fastest rotators observed by these authors in the young disc population (age ≈ 3 Gyr; Mayor 1974, Meusinger, Stecklum & Reimann 1991) were of ∼ M4 spectral type, with $P/\sin i \sim 12$ hours. Given that we expect the objects to spin-down on the main sequence, their origin must be in the most rapid rotators of the present sample (∼ 0.25 days), suggesting a factor of only ∼ 2 spin-down. This is slower than the Skumanich (1972) $t^{1/2}$ prediction of a factor of ∼ 4.5, suggestive of a very long spin-down timescale for these late-type dwarfs compared to solar-type dwarfs.

6 DISCUSSION
6.1 Link to angular momentum
It is instructive to examine the implications of the relations determined in §5.2.1 for the stellar angular momentum $J$. We define

$$J = I\omega$$

(7)

$$= \frac{2\pi k^2 MR^2}{P}$$

(8)

where $I = k^2 MR^2$ is the moment of inertia of a star of mass $M$ and radius $R$, $k$ is the radius of gyration (e.g. $k^2 = 2/5$ for a sphere of uniform density), and $\omega = 2\pi/P$ is the rotational angular velocity.

For a fully-convective star ($M \lesssim 0.4$ $M_\odot$), $k$ is approximately independent of mass, and therefore the specific angular momentum $j = J/M \propto R^2/P$. Furthermore, on the ZAMS we can approximate $M \propto R$ at these masses. Thus,

1 Fitting the mass-radius relation from the models of Baraffe et al. (1995) over the range $0.1 < M/M_\odot < 0.7$ with a simple linear model gave $R/R_\odot = 0.8M/M_\odot + 0.075$, which is a better approximation than the simple proportionality.
Figure 17. Rotation period as a function of stellar mass for (top to bottom): ONC, NGC 2264, NGC 2362, the Pleiades (rotation periods and \( v \sin i \) data on separate plots), NGC 2516 and M34. Lower and upper limits (from \( v \sin i \) data) are marked with arrows. The masses were taken from the NextGen mass-magnitude relations (Baraffe et al. 1998) at the appropriate ages. The ONC data are from Herbst et al. (2002). For NGC 2264 we used the data of Lamm et al. (2005) and Makidon et al. (2004). The NGC 2362 data are from the Monitor project, to be published in Hodgkin et al. (in prep). The Pleiades rotation period data are a compilation of the results from Van Leeuwen, Althaus & Moya (1987), Stauffer et al. (1987), Magnitskii (1987), Prosser et al. (1993a), Prosser et al. (1993b), Prosser et al. (1995), Krishnamurthi et al. (1998) (taken from the open cluster database), Terndrup et al. (1999) and Scholz & Eisloffel (2004). The Pleiades \( v \sin i \) data are a compilation of results from Stauffer et al. (1984), Stauffer & Hartmann (1987), Soderblom et al. (1993), Jones, Fischer & Stauffer (1996), Queloz et al. (1998) and Terndrup et al. (2000). The M34 data are taken from Irwin et al. (2004). In the NGC 2516

recalling the simple description of the morphology of the period versus mass plots in terms of power law relations in §5.2.1 and Figure 17, \( P = \) constant implies \( J \propto M^2 \), and \( P \propto M^3 \) implies \( J \propto M^{-1} \). These correspond to \( J \propto M^3 \) and \( J = \) constant, respectively. A plot of \( J \) as a function of stellar mass for the NGC 2516 sample is shown in Figure 18 with these lines overlaid.

We computed the median rotation period as a function of mass for the NGC 2516 data, finding it was consistent with \( P_{\text{med}} \propto M^2 \), a relation inbetween those of the upper and lower envelopes in Figure 17. This implies \( J = \) constant as a function of mass, a result consistent with the conclusions of Herbst, Bailer-Jones & Mundt (2001) in the ONC. The lack of any change in the median relation for stars still undergoing contraction on the PMS indicates that any mass-dependent angular momentum losses are not important in determining the evolution of the median over this age range. However, this is not the case in detail or once the stars reach the ZAMS, in particular the shape of the distribution even in this mass range does evolve in a mass-dependent fashion.

It is interesting to compare the present observations with the Pleiades survey of Scholz & Eisloffel (2004). The mass-dependence of the angular momentum evolution we have derived for NGC 2516 appears to be slightly inconsistent with their conclusions, where they found \( P \propto M \). Examining the Pleiades diagram in Figure 17 indicates that their result can most likely be attributed to the lack of data for \( 0.25 < M/M_\odot < 0.5 \). Otherwise the results of the surveys are in good agreement, as expected due to the similar ages of the two clusters.

The earlier conclusions of Scholz & Eisloffel (2004) in \( \sigma \) Ori (age \( \sim 3 \) Myr) are interesting, since they also found \( P \propto M \). At these ages, the mass-radius relation is better-fit by \( R/R_\odot \propto (M/M_\odot)^{1/2} \), so this implies \( P \propto R^2 \), or constant specific angular momentum, the same as our median relation.
6.2 Simple models

6.2.1 Description

We have developed a simple model scheme, to attempt to find an explanation for the observations, following the approach of Bouvier et al. (1997) and Allain (1998). In this work, the relation between $M$, $R$ and $K$ as a function of time for the radiative core (where present) and convective envelope was taken from the Lyon group stellar models, generously supplied to us by I. Baraffe (private communication) for 0.1, 0.2, 0.3, 0.4, 0.6, 0.8 and 1.0 $M_\odot$. We have interpolated the values where necessary for intermediate masses.

The overall angular momentum loss rate was split into two components: losses due to stellar winds, assuming a loss law with saturation at a critical angular velocity $\omega_{\text{sat}}$ (allowed to vary as a function of mass), and losses due to disc locking, which to a good approximation maintains a constant angular velocity until the circumstellar disc dissipates.

We assume an angular momentum loss law for stellar winds of the form suggested by Kawaler (1983), modified to include saturation of the angular momentum losses above a critical angular velocity $\omega_{\text{sat}}$. Barnes & Sofia (1996) argue that saturation at high velocity is required to account for fast rotators on the ZAMS, and may be physically motivated by saturation of the magnetic dynamo activity giving rise to the angular momentum losses. This is supported by observations of several diagnostics of magnetic activity, including saturation of chromospheric emission (e.g. Vilhu 1984).

The adopted angular momentum loss law has the following form:

\[
\frac{dJ}{dt}_\text{wind} = \begin{cases} 
-K \omega^3 \left( \frac{R}{R_*} \right)^{1/2} \left( \frac{M}{M_\odot} \right)^{-1/2}, & \omega < \omega_{\text{sat}} \\
-K \omega \omega_{\text{sat}}^2 \left( \frac{R}{R_*} \right)^{1/2} \left( \frac{M}{M_\odot} \right)^{-1/2}, & \omega \geq \omega_{\text{sat}}
\end{cases}
\]

where $\omega$ is the angular velocity of the star, $R$ is its radius, and $M$ its mass. $K$ is a constant, chosen to give the correct value of the solar angular momentum for a $1 M_\odot$ star at the age of the Sun. The value $K = 2.7 \times 10^{37}$ g cm$^2$ s was determined by Bouvier et al. (1997) to satisfy this requirement, with $\omega_{\text{sat}} = 14 \, \omega_\odot$. This particular form of angular momentum loss law is found to reproduce the time dependence of rotation between the Hyades age (625 Myr) and the Sun (4.57 Gyr).

The value of $\omega_{\text{sat}}$ is found to depend on stellar mass (e.g. Krishnamurthi et al. 1997, Barnes & Sofia 1996), and is typically assumed to be inversely proportional to the convective overturn timescale $\tau$: \[\omega_{\text{sat}} = \omega_{\text{sat}, \odot} \frac{\tau_\odot}{\tau}\] (10) where the quantities subscripted $\odot$ are those for the sun (Krishnamurthi et al. 1997). The values of $\tau$ were taken from the 200 Myr model of Kim & Demarque (1996) for $M > 0.5 M_\odot$. Sills, Pinsonneault & Tondrum (2000) found that simply linearly extrapolating these models to lower masses did not work well, and derived a set of empirical values to fit the distribution seen in the Hyades at these masses. We have also found this to be the case for the NGC 2516 data, and adopt the values of Sills et al. (2001), which give a much better fit to the data.

We consider two classes of models: solid body rotation, where the star is considered to rotate as a single solid body, implying that the core and envelope must have the same angular velocity, and differential rotation, where the core and envelope are allowed to decouple, with angular momentum losses from the envelope, and angular momentum transfer on a timescale $\tau_c$ between the core and envelope.

In order to account for disc locking, we introduce a disc locking time $\tau_{\text{disc}}$, such that for $t < \tau_{\text{disc}}$, the star is locked to the circumstellar disc, and maintains a constant angular velocity in the convective envelope, equal to the initial value. For $t > \tau_{\text{disc}}$, the angular velocity evolves as follows:

For solid body rotation, we can simply differentiate the expression $J = I \omega$ where $I$, $J$ and $\omega$ are the quantities for the entire star, with respect to time. The only angular momentum loss is due to stellar winds, so:

\[
\frac{d\omega}{dt} = \frac{\omega}{J} \left( \frac{dJ}{dt}\right)_\text{wind} - \frac{\omega}{\tau} \frac{dI}{dt}
\]

(11)

For differential rotation, the core and envelope must be considered separately. For the envelope, two extra terms are added (see Allain 1998 for a full derivation), describing the coupling of angular momentum from the core (first term), and the loss of mass to the core as the star evolves (second term):

\[
\frac{d\omega_{\text{conv}}}{dt} = \frac{1}{I_{\text{conv}}} \frac{\Delta J}{\tau_c} + \frac{2}{3} K \frac{R_*^2}{I_{\text{conv}}} \omega_{\text{conv}} \frac{dM_{\text{rad}}}{dt} - \frac{\omega_{\text{conv}}}{I_{\text{conv}}} \frac{dI_{\text{conv}}}{dt}
\]

where we assume:

\[
\Delta J = \frac{J_{\text{conv}} I_{\text{rad}} - J_{\text{rad}} I_{\text{conv}}}{I_{\text{rad}} + I_{\text{conv}}}
\]

(12)

as suggested by MacGregor (1991). The corresponding equation for the evolution of the core angular velocity is:

\[
\frac{d\omega_{\text{rad}}}{dt} = -\frac{1}{I_{\text{rad}}} \frac{\Delta J}{\tau_c} + \frac{2}{3} K \frac{R_*^2}{I_{\text{rad}}} \omega_{\text{conv}} \frac{dM_{\text{rad}}}{dt} - \frac{\omega_{\text{rad}}}{I_{\text{rad}}} \frac{dI_{\text{rad}}}{dt}
\]

(13)

where the first two terms again represent coupling of angular momentum to the envelope, and mass gained by the core (from the convective envelope), respectively. The final term accounts for the change in moment of inertia of the core as the star evolves.

6.2.2 Evolution from NGC 2362

We first attempt to evolve the observed rotation rates from our survey in NGC 2362 (Hodgkin et al., in prep) forward in time to reproduce the available rotation period data in NGC 2516. In order to do this, we consider the slowest rotators, characterised by the 25th percentile (the lower quartile) of the distribution of observed angular velocities, $\omega$, and the fastest rotators, characterised by the 90th percentile of the distribution. The discrepancy in measures here is because the 10 percentile was found to be somewhat unstable in the presence of small number statistics for slow rotators in some of the clusters under consideration. Nevertheless, the results for this quantity are compatible with the conclusions we draw for the 25 percentile for those clusters with sufficiently good statistics.

We fit solid body and differentially rotating models to the data, allowing the parameters $\omega_{\text{sat}}$, $\tau_{\text{disc}}$ and $\tau_c$ to vary to fit the slowest rotators (25 percentile).
Figure 19 shows our results, where we performed the analysis in a series of mass bins, in order to resolve the mass dependence of the evolution. These were: $0.9 < M/M_\odot \leq 1.1$, $0.7 < M/M_\odot < 0.9$, $0.5 < M/M_\odot \leq 0.7$, $0.35 < M/M_\odot \leq 0.5$, and $0.2 < M/M_\odot \leq 0.35$ (chosen empirically to encompass the changes in behaviour seen in the models, while retaining reasonable statistics). The models were calculated for single masses roughly at the centre of these bins, of $1.0, 0.8, 0.6, 0.42$ and $0.28$ $M_\odot$.

The solid body models shown in Figure 19 show good overall agreement with the upper 90 percentiles for the NGC 2516 data, in all the mass bins. For the $0.9 < M/M_\odot < 1.1$ bin, the M34 upper 90 percentile is at much greater $\omega$ than the model, but we suspect that this result is not significant due to small number statistics in the M34 sample at these masses: the discrepancy is due to the presence of 3 data points, and as discussed in Irwin et al. (2006), these may be contaminants. For $0.7 < M/M_\odot < 0.9$ the upper 90 percentile in the Hyades appears to lie at much greater $\omega$ than the model, but again this result is strongly affected by small number statistics. In order to resolve these issues, improved statistics at these masses and ages will be required. We note that the differentially rotating models with the assumed values of $\tau_s$ give a poor fit to the fast rotators (as characterised by the 90 percentiles), especially on the ZAMS.

For the lower 25 percentiles, the solid body models give a poor fit to the evolution from NGC 2362 to older ages, which becomes particularly apparent after $\sim 50$ Myr to the age of the Hyades in the top two mass bins. Introducing core-envelope decoupling with $\tau_c = 1.0$ Gyr provides a much better fit to the observations, and produces curves in good agreement with all the presently available data. We note however that we have not constrained these to fit the sun, which requires a modification of the constant $K$ in Eq. (9).

An interesting implication of the results in Figure 19 is that we cannot find a model in this scheme that fits both the slow and fast rotators simultaneously: the values of $\tau_c$ required in the models are different (solid body models correspond to $\tau_c = 0$). The result that the fast rotators seem to behave more like solid bodies may indicate that the redistribution of angular momentum at the core/envelope boundary is more efficient in fast rotators.

We note that there are relatively few constraints on the evolution for masses $< 0.7$ $M_\odot$ at the intermediate ages (5 to 150 Myr), and at old ages ($> 200$ Myr). We have recently obtained data in NGC 2547 ($\sim 38.5$ Myr; Naylor & Jeffries 2004) at these masses, which should allow us to address the first of these problems in a forthcoming publication.

6.2.3 Constraints on initial conditions

We explore here an alternative method for analysis of the NGC 2516 data, following Sills et al. (2000). By assuming that all stars share the same initial rotation rate, here 10 days, as used by Sills et al. (2000), we can constrain the disc lifetimes required to reproduce the observed envelope in diagrams of $\omega$ as a function of stellar mass. In particular, the observed lower envelope as a function of mass (the slowest rotators seen) must result from the longest disc lifetimes, and hence we can derive the required maximum disc lifetime as a function of mass. Figure 20 shows the results of this analysis for NGC 2516.

The results in Figure 20 indicate that the disc lifetime must decrease strongly as a function of decreasing mass in order to reproduce the NGC 2516 data with a single initial rotation period. Lifetimes of $> 10$ Myr are required for $M > 0.3$ $M_\odot$, a result at odds with other measurements (e.g. Haisch et al. 2001; Bouwman et al. 2000 and references therein), which indicate values of $\sim 10$ Myr at solar mass. Therefore it seems unlikely that the envelope shape we observe is due purely to varying disc lifetimes as a function of mass.

An alternative explanation (the other extreme) is that the initial period $P_0$ varies as a function of mass, but the disc lifetime $t_{\text{disc}}$ remains fixed. Figure 21 shows the results of doing this for the NGC 2516 data, assuming $t_{\text{disc}} = 10$ Myr, indicating again that a rather wide range of initial conditions appear to be required to explain the observed envelope purely by variations of $P_0$. Furthermore, the very slow rota-
Figure 19. Rotational angular velocity $\omega$ plotted as a function of time in five mass bins: $0.9 < M/M_\odot \leq 1.1$, $0.7 < M/M_\odot \leq 0.9$, $0.5 < M/M_\odot \leq 0.7$, $0.35 < M/M_\odot \leq 0.5$, and $0.2 < M/M_\odot \leq 0.35$. Crosses show the rotation period data, and short horizontal lines the 25th and 90th percentiles of $\omega$, used to characterise the slow and fast rotators respectively. The lines show our models for 1.0, 0.8, 0.6, 0.42 and 0.28 M$_\odot$ (respectively), where the solid lines are solid body models, and dashed lines are differentially rotating models, with the parameters shown. Plotted are the ONC (1 Myr), NGC 2264 (2 Myr), NGC 2362 (5 Myr), IC 2391, IC 2602 (∼30 Myr), α Per (∼50 Myr), NGC 2516, M34, the Hyades (625 Myr) and the Sun (∼4.57 Gyr). The IC 2391 data were taken from Patten & Simon (1996) and IC 2602 from Barnes et al. (1999). The α Per data are a compilation of the results from Stauffer et al. (1985), Stauffer, Hartmann & Jones (1988), Prosser et al. (1993a), Prosser (1991), Prosser et al. (1993b), O’Dell & Collier Cameron (1993), Prosser et al. (1995), O’Dell, Hendry & Collier Cameron (1994), O’Dell et al. (1996), Allain et al. (1996), Martín & Zapatero Osorio (1997), Prosser & Randich (1998), Prosser, Randich & Simon (1998), Barnes et al. (1998), and the Hyades data from Radick et al. (1987) and Prosser et al. (1995), taken from the open cluster database.

6.2.4 Value of $\omega_{\text{sat}}$

The value of $\omega_{\text{sat}}$ at each mass is tightly constrained by the need to reproduce the NGC 2516, M34 and Hyades data. In 6.2.2 we derived values for $\omega_{\text{sat}}$ in coarse mass bins, to
produce model curves providing a reasonable explanation for the observations. In order to investigate the mass dependence of this parameter in detail, we used the NGC 2362 and NGC 2516 observations to perform a fit of \( \omega_{\text{sat}} \) as a function of mass in much smaller bins to give better sampling, using the same percentile based technique. Figure 22 shows the results, finding a linear dependence of \( \omega_{\text{sat}} \) on mass to be a good approximation at the lowest masses, for both solid body and differentially rotating models. There is some evidence that the relation does not apply for higher masses (\( M > \sim 0.5 \, M_{\odot} \)), but in reality \( \omega_{\text{sat}} \) is not well-constrained here, since the majority of these stars (which are slow rotators) only reach the saturation velocity for a short time during the evolution from 5 to 150 Myr.

From the fit, at solar mass, \( 0.8 \, M_{\odot} \) and \( 0.5 \, M_{\odot} \), the relation gives \( \omega_{\text{sat}} = 14.3, 11.1, 6.3 \, \omega_{\odot} \) respectively for the solid body models, and \( \omega_{\text{sat}} = 11.9, 9.35, 5.61 \, \omega_{\odot} \) for the differentially rotating models. The value for solar mass and solid body rotation is very close to the value of 14 \( \omega_{\odot} \) we assumed earlier, as derived from the convective turnover timescale, but at 0.8 and 0.5 \( M_{\odot} \), \( \omega_{\text{sat}} \) is larger than the values of 8 \( \omega_{\odot} \) and 3 \( \omega_{\odot} \) predicted by Eq. (10); the slope of \( \omega_{\text{sat}} \) as a function of mass is less steep than predicted from the convective turnover timescale.

The decrease of \( \omega_{\text{sat}} \) with decreasing mass, as determined in this work, effectively reduces the amount of angular momentum loss experienced by lower mass stars, compared to what would be experienced if the value was the same as at solar mass. This has also been seen in previous work, e.g. Barnes & Sofia (1996).

6.2.5 Detailed evolution

Figure 23 shows the results of attempting to evolve the measured rotation periods in NGC 2362 forward in time to the age of NGC 2516 using the models we have described, with the relations fit from Figure 22 for \( \omega_{\text{sat}} \) as a function of mass, on an object-by-object basis. By doing this, we can test if the model we have presented can reproduce the observations of NGC 2516, given the NGC 2362 rotators as input. Note that we have neglected disc locking in this analysis for simplicity.

The apparent mass dependent morphology of the NGC 2516 distribution is well-reproduced from the NGC 2362 distribution by the models, with two exceptions: the slow rotators at the highest masses in the diagram, the predicted

\[ \omega_{\text{sat}} / \omega_{\odot} = 16.0 (M/M_{\odot}) - 1.7 \] (solid body models) and \( \omega_{\text{sat}} / \omega_{\odot} = 12.5 (M/M_{\odot}) - 0.6 \) (differentially rotating models).

Figure 22. \( \omega_{\text{sat}} \) plotted as a function of mass, in 0.1 \( M_{\odot} \) bins, from fitting to the NGC 2516 j distribution lower 25 percentile (plus symbols) and upper 90 percentile (stars), using NGC 2362 as the initial condition, for solid body models (top) and differentially rotating models (bottom; \( \tau_c = 1.0 \) Gyr). This diagram indicates that a single functional form fails to fit all of these measures simultaneously for \( M > \sim 0.5 \, M_{\odot} \), but that a simple linear relation is a good approximation at lower masses. The straight lines show a fit for \( M \leq 0.5 \, M_{\odot} \), finding \( \omega_{\text{sat}} / \omega_{\odot} = 16.0 (M/M_{\odot}) - 1.7 \) (solid body models) and \( \omega_{\text{sat}} / \omega_{\odot} = 12.5 (M/M_{\odot}) - 0.6 \) (differentially rotating models).

\[ \omega_{\text{sat}} / \omega_{\odot} = 16.0 (M/M_{\odot}) - 1.7 \] (solid body models) and \( \omega_{\text{sat}} / \omega_{\odot} = 12.5 (M/M_{\odot}) - 0.6 \) (differentially rotating models).

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A small number of objects are also visible in the evolved NGC 2362 distribution above the $P \propto M^3$ relation seen for the slowest rotators in NGC 2516. Since these originated as relatively slow rotators in NGC 2362, we suspect that they are the result of field contamination, or errors in the measured rotation periods in that sample due to the limited time baseline of the observations.

This work suggests that the mass dependence of the observed rotation period distribution is reproduced by the combination of the initial conditions as seen in NGC 2362, the mass-dependence of stellar contraction on the PMS, and the mass-dependence of the saturation angular velocity $\omega_{\text{sat}}$. Furthermore, the convergence in rotation rates as a function of time (see also Figure 19) is explained reasonably well by saturation of the angular momentum losses, over the mass range of interest for NGC 2516, apparently without need to invoke any further effects.

Figure 24 shows the same comparison for M34, showing that the feature of constant rotation period as a function of mass for $M \gtrsim 0.6 \, M_\odot$ is also well-reproduced by the models, at approximately the correct period in the case of the differentially rotating models, and again at a shorter period than the observed value for the solid body models. It should be noted that the adopted values of $\omega_{\text{sat}}$ in this mass range are not well-constrained by the NGC 2516 data used to calibrate them, and have a strong effect on the morphology of this part of the diagram, so it is possible that any deviations here result from our assumption of a linear relation over the entire mass range.

7 CONCLUSIONS

We have reported on results of an $i$-band photometric survey of NGC 2516, covering $\sim 1$ sq.deg of the cluster. Selection of candidate members in a $V$ versus $V-I$ colour-magnitude diagram using an empirical fit to the cluster main sequence found 1685 candidate members, over a $V$ magnitude range of $16 < V < 26$ (covering masses from $0.7 \, M_\odot$ down to below the brown dwarf limit). The likely field contamination level was estimated using a simulated catalogue of field objects from the Besançon Galactic models (Robin et al. 2003), finding that $\sim 650$ objects were likely field contaminants, an overall contamination level of $\sim 39\%$, implying that there are $\sim 1000$ real cluster members over this mass range in our field-of-view.

From $\sim 8$ nights of time-series photometry we derived lightcurves for $\sim 104000$ objects in the NGC 2516 field, achieving a precision of $< 1\%$ per data point over $15 < i < 19$. The lightcurves of our candidate cluster members were searched for periodic variability corresponding to stellar rotation, giving 362 detections over the mass range $0.15 < M/M_\odot < 0.7$.

A striking morphology was found in the rotation period distribution as a function of both mass, with a median relation of $P \propto M^2$ (or constant specific angular momentum $j$) for masses below $\sim 0.6 \, M_\odot$, with the slowest rotators (the majority of the sample) following $P \propto M^3$ ($j \propto M^{-1}$), with the fastest rotators over the entire mass range having $P \gtrsim 0.25$ days (corresponding to a line of $j \propto M^2$). Our earlier M34 results indicate that for $M \gtrsim 0.6 \, M_\odot$, the slowest rotators follow instead $P \sim$ constant as a function of mass.

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Figure 23. Rotation period as a function of mass, using the model presented in §6.2 to evolve the NGC 2362 distribution of Figure 17 forward in time from 5 Myr to 150 Myr for the solid body (upper panel) and differentially rotating (middle panel) models, and the observed NGC 2516 distribution for comparison (lower panel).
with a transition between the two regimes at \( M \sim 0.6 \, M_\odot \).

We suggest that this mass corresponds to the transition to convectively-dominated stellar interiors moving to lower masses. This could be tested by examining rotation period distributions over a wider range of ages for M-dwarfs.

In §6.2 simple models of the rotational evolution were considered, both for the solid body case, and including differential rotation between a decoupled radiative core and convective envelope, following Bouvier et al. (1997) and Allain (1998). A Kawaler (1988) angular momentum loss law incorporating saturation at a critical angular velocity \( \omega_{\text{sat}} \) was assumed. The results indicate that a mass-dependent saturation velocity (e.g. of the form suggested by Sills et al. 2000) is required to reproduce the observations. Furthermore, we find that solid body rotation is sufficient to explain the evolution of the fastest rotators, but core-envelope decoupling appears to be needed to explain the evolution of the slowest rotators. This may indicate that the redistribution of angular momentum at the core/envelope boundary is more efficient in fast rotators. We were unable to find a model which fits both the fast and slow rotators simultaneously. Further rotation period measurements at low masses, particularly for ages intermediate between 5 and 150 Myr and for ages > 200 Myr, will provide more stringent constraints on the models, but the present observations already indicate the need for more theoretical work.

We intend to publish the final catalogue of NGC 2516 membership candidates after obtaining follow-up spectroscopy. However, the preliminary catalogue of membership candidates is available on request.

**ACKNOWLEDGMENTS**

Based on observations obtained at Cerro Tololo Inter-American Observatory, a division of the National Optical Astronomy Observatories, which is operated by the Association of Universities for Research in Astronomy, Inc. under cooperative agreement with the National Science Foundation. This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation. This research has also made use of the SIMBAD database, operated at CDS, Strasbourg, France. The Open Cluster Database, as provided by C.F. Prosser and J.R. Stauffer, may currently be accessed at http://www.noao.edu/noao/staff/cprosser/ or by anonymous ftp to 140.252.1.11, cd/pub/prosser/clusters/.

JI gratefully acknowledges the support of a PPARC studentship, and SA the support of a PPARC postdoctoral fellowship. We would like to express our gratitude to Isabelle Baraffe for providing the stellar evolution model tracks used in §6.2 and to the anonymous referee for comments that have helped to improve the paper.

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