Coordinated Multipoint (CoMP) Transmission Design for Cloud-RANs with Limited Fronthaul Capacity Constraints

Vu Nguyen Ha, Student Member, IEEE, Long Bao Le, Senior Member, IEEE, and Ngoc-Dung Dao, Member, IEEE

Abstract—In this paper, we consider the CoMP transmission design for the downlink cloud radio access network (Cloud-RAN). Our design aims to optimize the set of remote radio heads (RRHs) serving each user as well as the precoding and transmission powers to minimize the total transmission power while maintaining the fronthaul capacity and users’ QoS constraints. The fronthaul capacity constraint involves a non-convex and discontinuous function which renders the optimal exhaustive search method unaffordable for large networks. To address this challenge, we propose two low-complexity algorithms. The first pricing-based algorithm solves the underlying problem through iteratively tackling a related pricing problem while appropriately updating the pricing parameter. In the second iterative linear-relaxed algorithm, we directly address the fronthaul constraint function by iteratively approximating it with a suitable linear form using a conjugate function and solving the corresponding convex problem. For performance evaluation, we also compare our proposed algorithms with two existing algorithms in the literature. Finally, extensive numerical results are presented which illustrate the convergences of our proposed algorithms and confirm that our algorithms significantly outperform the state-of-the-art existing algorithms.

Index Terms—Cloud radio access network (Cloud-RAN), precoding, power minimization, resource allocation, limited fronthaul capacity.

I. INTRODUCTION

The next generation wireless cellular network is expected to provide significantly enhanced capacity to support the exponential growth of mobile data traffic [1–5]. Toward this end, Coordinated multipoint (CoMP) transmission/reception techniques provide promising solutions, which have been adopted in the LTE-Advanced standard [6]. In fact, CoMP employs different forms of BS coordination with dynamic sharing of channel state information (CSI) and/or data information among BSs as well as efficient transmission, precoding, and resource allocation algorithms [7]. However, implementation of CoMP in wireless cellular networks typically requires costly high-speed backhauls connecting different BSs for CSI and information exchanges and distributed computation [8, 9].

Cloud-RAN has been recently proposed as an alternative network architecture that can achieve the performance gains of the CoMP techniques while effectively exploiting the computation power of the cloud computing technology. In Cloud-RAN, the cloud comprising a pool of baseband processing units (BBUs) performs most base-band processing tasks while transmission functions are realized by simple RRHs using the processed baseband signals received from the cloud through a fronthaul transport network [10–13]. With centralized cloud processing center (CPC), complex resource allocation optimization such as precoding, power control, user scheduling, interference management algorithms can be realized, which can translate into significant network performance improvements. In addition, the Cloud-RAN with simple RRHs enables us to reduce both capital and operational expenditure of the network [12]. Moreover, this emerging network architecture also allows to deploy dense small-cells efficiently [14].

Despite these benefits, there are various technical challenges one must resolve in designing and deploying the Cloud-RAN architecture. In particular, suitable mechanisms that efficiently utilize computing resources in the cloud, fronthaul capacity to realize advanced communications, baseband signal processing, and resource allocation schemes must be developed. There are some recent works that address some of these issues as can be described in the following. In [15], Fan et al. propose an efficient clustering algorithm to reduce the number of computations in the centralized pool of BBUs where the number of RRHs is very large. The works in [16, 17] develop compression techniques to minimize the amount of data transmitted over the fronthaul transport network.

Several other papers focus on precoding/decoding design for CoMP considering different design aspects of Cloud-RAN. In particular, Liu and Lau in [18] study the joint optimization of antenna selection, regularization, and power allocation to maximize the average weighted sum-rate. The random matrix theory is utilized to decompose the considered non-convex problem into sub-problems which can be tackled more easily. The works [19, 20] optimize the precoding vectors for all RRHs to minimize the total network power consumption where [19] considers the downlink while [20] addresses both downlink and uplink communications. Total power to support radio transmission and operations of fronthaul links and RRHs is accounted for in these research works where the authors show how to transform the underlying problems into the sparse beamforming problems. Then, these papers combine the

Copyright © 2015 IEEE. Personal use of this material is permitted. However, permission to use this material for any other purposes must be obtained from the IEEE by sending a request to pubs-permissions@ieee.org.

Manuscript received February 3, 2015; revised June 4, 2015; revised September 16, 2015; accepted September 23, 2015.

Vu Nguyen Ha and Long Bao Le are with INRS, Université du Québec, Montreal, QC, Canada; e-mails: {hanguyen, long.le}@emt.inrs.ca.

Ngoc-Dung Dao is with Huawei Technologies Canada Co. Ltd., Ottawa, Canada; e-mail: Ngoc.Dao@huawei.com.
solution techniques employed to address the traditional power minimization problem in [21, 22] and the fronthaul capacity minimization problem in [23] to tackle the transformed problem. This solution technique is also closely related to that employed in [24]. In fact, the design problems considered in [23, 24] for CoMP and in [19, 20] for Cloud-RAN with standard convex constraints do not explicitly model the fronthaul capacity constraints. Consequently, they can be solved directly by employing the compressed sensing techniques [26–28]. We would like to emphasize that the related work [23] aims at minimizing the number of active links between base stations (RRHs) and users. Therefore, the limited fronthaul capacity is not explicitly imposed as constraints in [23] but it is rather considered in the design objective. Note that the greedy principle proposed in [23] can be employed to solve our problem (even though our problem is not the same with the problem in [23]); however, such greedy approach may not achieve very good performance.

This current work aims to study the CoMP joint transmission design problem for Cloud-RAN that explicitly considers the fronthaul capacity as well as users’ QoS constraints. In particular, we make the following contributions.

- We formulate the joint transmission design problem for Cloud-RAN which optimizes the set of RRHs serving each user together with their precoding and power allocation solutions to minimize the total transmission power considering users’ QoS and fronthaul capacity constraints. In particular, we assume that certain fronthaul capacity, which depends on the user’s required QoS, is consumed to transfer the processed baseband signal from the cloud to one particular RRH serving that user and that the fronthaul transport network has limited capacity. The considered problem is indeed non-convex and it comprises the discontinuous fronthaul capacity constraint as well as other traditional power and users’ QoS constraints. Therefore, addressing this problem through exhaustive search requires exponential computation complexity, which is not affordable for practically large networks.

- To tackle the considered problem, we then develop two different low-complexity algorithms. For the first algorithm, named Pricing-Based Algorithm, we consider the related pricing problem and devise a novel mechanism to iteratively update the pricing parameter to obtain a good feasible solution. The second algorithm, called Iterative Linear-Relaxed Algorithm, is developed by regularizing the fronthaul constraint function into an approximated linear form and iteratively solving the approximated optimization problem.

- For performance comparison, we also describe two existing algorithms proposed in [23] and [25] (with appropriate modifications due to different considered settings), which can also solve our considered problem. We then study the extended setting where there are multiple individual fronthaul capacity constraints. We show that it is possible to adapt the proposed low-complexity algorithms to solve the corresponding problem in this setting. In addition, we indicate the need to introduce multiple pricing parameters each of which is required to deal with one corresponding fronthaul capacity constraint in the extended Iterative Linear-Relaxed Algorithm.

- Numerical results are presented to demonstrate the efficacy of the proposed algorithms and their relative performance compared to the optimal algorithm and existing algorithms. We show the convergence and the impacts of parameters such as number of users, number of antennas, users’ QoS constraints, and fronthaul capacity on the network performance. Specifically, while both two proposed algorithms perform remarkably well in most cases, the pricing-based algorithm achieves slightly better performance than the iterative linear-relaxed algorithm at the cost of longer convergence time. In addition, both proposed algorithms significantly outperform the existing algorithms in [23] and [25] for all considered simulation scenarios.

The remaining of this paper is organized as follows. We describe the system model and problem formulation in Section II. In Section III, we present three low-complexity algorithms. Next, we extend our proposed algorithms to the setting with multiple individual fronthaul capacity constraints and the MIMO systems where multiple data streams can be transmitted to each user in Section IV. Numerical results are presented in Section V followed by conclusion in Section VI. Some preliminary results of this paper have been published in [29] and [30].

For notation, we use $X^T$, $X^H$, $\text{Tr}(X)$ and $\text{rank}(X)$ to denote transpose, Hermitian transpose, trace, and rank of matrix $X$, respectively. $1_{x \times y}$, $0_{x \times y}$ denote the matrix of ones, matrix of zeros whose dimension are $x \times y$, respectively. $|S|$ denotes the cardinality of set $S$ and $\text{diag}(x)$ is the diagonal matrix constructed from the elements of vector $x$.

II. SYSTEM MODEL AND PROBLEM FORMULATION

A. System Model

The general architecture of Cloud-RAN under consideration as illustrated in Fig. 1 consists of three main components: (i) CPC consisting BBUs pool, (ii) the optical fronthaul transport network (i.e., fronthaul links), and (iii) RRH access units with antennas located at remote sites. Specifically, the CPC comprising a certain number of BBUs is the heart of this architecture where BBUs act as virtual base stations that process baseband signals for users and optimize the network resource allocation tasks. The fronthaul transport network connecting the CPC and distributed RRHs is usually deployed using optical fibers. In addition, RRHs communicate with users in the downlink via RF signals, which are formed by using the baseband signals and the precoding vectors received from the BBU pool.

In this paper, we consider the joint transmission design for CoMP downlink communications in the Cloud-RAN with $K$ RRHs and $M$ users. Let $K$ and $U$ be the sets of RRHs and users in the network, respectively. Suppose that RRH $k$ is equipped with $N_k$ antennas ($k \in K$) and each user has a single antenna. We assume that each user is served by a specific group of assigned RRHs and one RRH can serve a number
of users. When RRH \( k \) is assigned to serve user \( u \), this RRH receives the user’s processed baseband signal from the cloud. Then, the RRH converts and transmits the corresponding RF signal using a suitably designed precoding vector. Also, denote \( v^k_u \in \mathbb{C}^{N_k \times 1} \) as the precoding vector at RRH \( k \) corresponding to the signal transmitted to user \( u \). Then, the transmission power used by RRH \( k \) to serve user \( u \) can be expressed as

\[
p^k_u = v^k_u v^H_k.
\]  

(1)

Let \((k, u)\) represent the communication link between RRH \( k \) and user \( u \). For simplicity, we assume that each user is virtually served by all RRHs in all expressions and problem formulations. However, a user is actually served by one particular RRH if the corresponding transmission power is strictly larger than zero. Let \( x_u \in \mathbb{C} \) denote the signal symbols with unit power for user \( u \), which are transmitted by RRHs in set \( K \) upon receiving the processed baseband signals from the cloud. Then, the baseband signal \( y_u \) received at user \( u \) can be written as

\[
y_u = \sum_{k \in K} h^H_{u,k} v^k_u x_u + \sum_{i=1, i \neq u \in K} M \sum_{l \in K} h^H_{u,l} v^l_i x_i + \eta_u,
\]  

(2)

where \( h^H_{u,k} \in \mathbb{C}^{N_k \times 1} \) denotes the channel vector between RRH \( k \) and user \( u \), and \( \eta_u \) describes the noise at user \( u \). Then, the SINR achieved by user \( u \) can be described as

\[
\Gamma_u = \frac{\sum_{k \in K} h^H_{u,k} v^k_u}{\sum_{i=1, i \neq u \in K} M \sum_{l \in K} h^H_{u,l} v^l_i + \sigma^2},
\]  

(3)

where \( \sigma^2 \) is the noise power. In this paper, we are interested in design the precoding in order to satisfy users’ QoS. This QoS constraint of user \( u \) is expressed as

\[
\Gamma_u \geq \gamma_u, \quad \forall u \in \mathcal{U},
\]  

(4)

where \( \gamma_u \) denotes the target SINR of user \( u \).

To manage the computation complexity in large networks, we can impose additional constraints where each user \( u \) can only be served by set of near RRHs \( \mathcal{R}_u \) (e.g., clustering constraints). This set of RRHs can be determined based on the distance or channel gain from them to each user.\(^1\)

\(^1\)For example, each user is potentially associated with \( r \) nearest RRHs as \( r^{th} \)-order Voronoi tessellation [34], or RRHs with strong channel gain as [35].

In the following, we assume that only RRH-user communications links in predetermined set \( \mathcal{L} \) are allowed where \( \mathcal{L} = \{(k, u) | u \in \mathcal{U}, k \in \mathcal{R}_u\} \). When no such constraint exists, set \( \mathcal{L} \) comprises all possible \( MK \) links between \( K \) RRHs and \( M \) users. We can express the relation between transmission power and communication link \((k, u)\) as follows:

\[
p^k_u = v^H_k v^k_u = 0 \quad \text{if} \quad (k, u) \notin \mathcal{L}.
\]  

(5)

Remark 1. In this paper, we assume that perfect channel state information (CSI) between all RRHs and users is available at the CPC. In practice, the CSI can be estimated by corresponding users and RRHs and then transferred to the CPC through the fronthaul network.\(^2\) In general, the transfer of CSI to the CPC over the fronthaul network consumes much smaller fraction of fronthaul capacity compared to the transfer of users’ data (i.e., I/Q data sequences) from the cloud to the RRHs. Moreover, the transfer of CSI can be performed periodically since the CSI would change slowly over time while the data transfer over the fronthaul network occurs continuously. Therefore, we do not explicitly consider the fronthaul capacity consumption due to CSI transfer in this paper, which is left for our future works.

1) Fronthaul Capacity: Let \( p^k = [p^k_1, ..., p^k_M]^T \) be the transmission power vector of RRH \( k \) whose elements \( p^k_u \geq 0 \) represent transmission power \( p^k_u \) given in (1). We also define the vector \( p = [p^T_1, ..., p^T_K]^T \) to describe the transmission powers of all RRHs for all users. Recall that \( p^k_u = 0 \) implies that RRH \( k \) does not serve user \( u \). In contrast, if \( p^k_u > 0 \), the fronthaul link from RRH \( k \) to user \( u \) is activated for carrying the baseband signal to serve user \( u \) at its required target SINR. Therefore, the total capacity of the fronthaul links can be indicated by the value of vector \( p \) and the target SINR of users, which can be written mathematically as

\[
G(p) = \sum_{k \in \mathcal{K}} \sum_{u \in \mathcal{U}} \delta(p^k_u) R^k_{th},
\]  

(6)

where \( \delta(\cdot) \) denotes the step function, and \( R^k_{th} \) represents the required capacity for transferring the signal of user \( u \) over the fronthaul network to the RRH \( k \). The required fronthaul capacity \( R^k_{th} \) depends on the actual required data rate corresponding to the target SINR \( \gamma_u \), the specific design of Cloud-RAN, and the specific quantization technique employed to process the baseband signals, which are discussed in the following remark.

Remark 2. In the Cloud-RAN downlink system, the CPC processes the baseband signals and optimizes the precoding vectors. As described in [38, 39], there are two strategies to realize such design, namely “Compression-After-Precoding” (CAP) and “Compression-Before-Precoding” (CBP). In the CAP, which is employed in [16, 17], the CPC precodes the data streams of users with their corresponding precoding vectors, then compresses the resulting signals and forwards them to the corresponding RRHs over the fronthaul network.

\(^2\)Detailed realization of CSI channel estimation varies depending if the time division duplex (TDD) or frequency division duplex (FDD) strategy is employed. In particular, in the TDD system, RRHs perform CSI estimation then they transfer the estimated CSI to the CPC.
For the CBP, the CPC directly compresses the precoding vectors and forwards the compressed vectors as well as users’ data streams to the corresponding RRHs [38]. Then, the RRHs precode the signals and transmit to users.

In this paper, we assume that the CBP strategy is employed, which is motivated by its advantages for the Cloud-RAN system with preliminary clustering [39]. In this strategy, information streams and precoding vectors are compressed and transmitted from the cloud to RRHs separately. The fronthaul capacity consumed by each RRH depends on the group of users it serves which is given in (6). In particular, the required fronthaul capacity to support the communication link between user $u$ to RRH $k$ can be calculated as

$$R_u^{k,\text{fh}} = R_u^{k,\text{pr}} + R_u^{k,\text{dt}}(\gamma_u),$$

where $R_u^{k,\text{dt}}(\gamma_u)$ and $R_u^{k,\text{pr}}$ correspond to the fronthaul capacity consumptions for transferring the information stream and precoding vector $v_u^k$ for user $u$ as given in equation (3) of [38], respectively. In fact, $R_u^{k,\text{dt}}(\gamma_u)$ is a function of the target SINR (e.g., it can be expressed $R_u^{k,\text{dt}}(\gamma_u) = \log_2(1 + \gamma_u)$ if the capacity can be achieved) and $R_u^{k,\text{pr}}$ can be predetermined based on the desirable quantization quality of precoding vectors. When the precoding vectors are quantized, and then employed at RRHs, there are the quantization errors. However, if the corresponding quantization noise is sufficiently small compared to the interference and noise at receivers, the quantization errors can be omitted which is what to be assumed in this paper.

Note that our model allows to capture the scenario where users demand services with different rate requirement (e.g., voice and video services). We are now ready to describe the considered Fronthaul–Constrained Power Minimization (FCPM) problem in the following.

**B. Problem Formulation**

We are interested in determining the set of RRHs serving each user and the corresponding precoding vectors (i.e., $\{v_u^k\}$) to minimize the total transmission power considering the constraints on fronthaul capacity limit, transmission power, and users’ QoS. Beside the SINR constraints in (4), we also impose the constraint on total transmission power for each RRH $k$ as

$$\sum_{u \in U} p_u^k = \|p^k\|_1 = \sum_{u \in U} v_u^k H v_u^k \leq P_k, \quad \forall k \in K, \quad (8)$$

where $P_k (k \in K)$ denotes the maximum power of RRH $k$, $\|x\|_1$ represents the $l_1$-norm of vector $x$. Furthermore, we assume that the capacity of fronthaul transport network between the cloud and all RRHs is limited and we denote $C$ as the fronthaul capacity limit. Then, we have to impose the following fronthaul capacity constraint

$$G(p) = \sum_{k \in K} \sum_{u \in U} \delta(p_u^k) R_u^{k,\text{fh}} \leq C. \quad (9)$$

This indeed represents the sum fronthaul capacity constraint. We will discuss the extended setting with multiple individual fronthaul capacity constraints in Section IV. Now, it is ready to state the FCPM problem as follows:

$$\min \{\gamma_u^k\} \mathcal{P}_{\text{FCPM}} \quad \|p\|_1$$

s. t. constraints (1), (4), (5), (8), (9).

We will describe how to transform this problem into an appropriate form based on which we can determine its optimal solution in the following.

1) **Optimal Exhaustive Search Algorithm:** The main challenge involved in solving problem $\mathcal{P}_{\text{FCPM}}$ comes from the fronthaul capacity constraint (9). Let us now define variables $a_u^k \in \{0, 1\}$ where $a_u^k = 1$ if RRH $k$ serves user $u$ and $a_u^k = 0$ otherwise. Denote $a$ as the allocation vector $[a_1^1, ..., a_K^M]$ and $S_a$ as the set of all possible $a$. Then, the consumed fronthaul capacity corresponding to a given vector $a$ can be written as

$$G(a) = \sum_{k \in K} \sum_{u \in U} a_u^k R_u^{k,\text{fh}}. \quad (11)$$

Then, we have to optimize over both integer variables $a \in S_a$ and continuous variables $\{v_u^k\}$ to find the optimal solution of the considered problem so that $G(a) \leq C$. Note, however, that the number of elements in set $S_a$ is finite. Also, suppose that the values of $a$ which satisfy constraint (9), are given, then we only need to solve following precoding optimization problem

$$\min \{\gamma_u^k\} \mathcal{P}_a \quad \sum_{k \in K} \sum_{u \in U} v_u^k H v_u^k$$

s. t. constraints (4), (8),

$$v_u^k H v_u^k = 0 \text{ if } a_u^k = 0, \quad \forall (u,k). \quad (12)$$

This problem is indeed the sum-power minimization problem (SPMP), which can be transformed into a solvable convex Semi-Definite Program (SDP). This transformation is described in Appendix A. Here, we refer to such a SPMP for given $a$ as a sparse–PMP. It is now clear that the optimal solution for problem $\mathcal{P}_{\text{FCPM}}$ can be determined as follows. First, we enumerate all possible $a$ that satisfy the fronthaul capacity constraints (9). Second, for each such feasible $a$, we solve the corresponding problem $\mathcal{P}_a$ and obtain the optimal precoding vectors and objective value. Finally, the feasible $a$ that achieves the minimum total transmission power together with the corresponding optimal precoding vectors are the optimal solution of problem $\mathcal{P}_{\text{FCPM}}$.

Such exhaustive search method, however, has exponentially high complexity. This motivates us to develop low-complexity algorithms to solve problem $\mathcal{P}_{\text{FCPM}}$ which is the focus of the following section.

**III. LOW-COMPLEXITY ALGORITHMS**

In this section, we describe two low-complexity algorithms with different levels of complexity to solve problem $\mathcal{P}_{\text{FCPM}}$. For the performance evaluation purposes, we also present two existing algorithms in [23] and [25].
A. Pricing-based Algorithm

The first low-complexity algorithm is developed by employing the penalty method to deal with the step-function fronthaul capacity constraint. Specifically, we consider the so-called Pricing Fronthaul Capacity and Power Minimization (PFPCM) problem, which is given in the following

\[
(P_{\text{PFPCM}}) \quad \min_{\{v^k_u\}, p} \|p\|_1 + qG(p) \\
\text{s. t. constraints (1), (4), (5), (8)}.
\]

In this problem, the consumed fronthaul capacity \(G(p)\) scaled by a pricing parameter \(q\) is added to the objective function of problem \(P_{\text{PFPCM}}\) and we have removed the fronthaul capacity constraint \((9)\). We can obtain a good feasible solution for problem \(P_{\text{PFPCM}}\) by iteratively solving problem \(P_{\text{PFPCM}}\) while adaptively adjusting the pricing parameter \(q\) so as to satisfy the fronthaul capacity constraint \((9)\). We describe this procedure in details in the following.

1) Relationship between FCPM and PFPCM Problems: We now establish the relationship between problems \(P_{\text{FCPM}}\) and \(P_{\text{PFPCM}}\) based on which we can develop an efficient algorithm to solve problem \(P_{\text{PFPCM}}\). Let \(G_{\text{PFPCM}}(q)\) be the consumed fronthaul capacity resulted from solving problem \(P_{\text{PFPCM}}\) for a given price parameter \(q\). Then, it can be verified that the optimal precoding vectors and the transmission powers of problems \(P_{\text{FCPM}}\) and \(P_{\text{PFPCM}}\) are the same if \(G_{\text{PFPCM}}(q) = C\). This fact enables us to develop an iterative algorithm to solve problem \(P_{\text{PFPCM}}\) through tackling problem \(P_{\text{PFPCM}}\) while adjusting \(q\) iteratively in attempting to attain \(G_{\text{PFPCM}}(q) = C\). Our proposed algorithm is developed based on the assumption that problem \(P_{\text{PFPCM}}\) can be solved, which will be addressed in the next subsection. In the following, we establish some theoretical results based on which we develop the mechanism to update the pricing parameter.

Proposition 1. Let \(\sigma_{\min}\) be the smallest non-zero value of \(|G(a) - G(a')|\) where \(\{a, a'\} \subset S_a\), and \(\bar{q} = \sum_{k \in K} P_k / \sigma_{\min}\). We have:

1) \(G_{\text{PFPCM}}(q)\) is a decreasing function of \(q\).
2) If we increase \(q \geq \bar{q}\) then \(G_{\text{PFPCM}}(q)\) cannot be further decreased.
3) When \(q \geq \bar{q}\), if \(G_{\text{PFPCM}}(q) > C\), problem \(P_{\text{PFPCM}}\) is infeasible.

Proof. The proof is given in Appendix B.

These results form the foundation based on which we can develop an iterative algorithm presented in Algorithm 1. In fact, we have described how the pricing parameter \(q\) is updated over iterations, which can be summarized as follows. At the first iteration, \(q^{(0)}\) is set equal to \(\bar{q}\) to verify the feasibility of problem \(P_{\text{PFPCM}}\). If \(G_{\text{PFPCM}}(\bar{q}) > C\), we can conclude that problem \(P_{\text{PFPCM}}\) is infeasible. Otherwise, we apply the bisection search method to update \(q\) until \(G_{\text{PFPCM}}(q) = C\).

2) PFPCM Problem Solution: We now develop an efficient algorithm to solve problem \(P_{\text{PFPCM}}\) based on concave approximation of step function. Note, the step function makes the objective function of problem \(P_{\text{PFPCM}}\) non-smooth, which is difficult to solve. To overcome this challenge, the step function \(\delta(x)\) for \(x \geq 0\) can be approximated by a suitable concave function. Denote \(f_{\text{apx}}^{k,u}(p^k_u)\) as the concave penalty function that approximates the step function \(\delta(p^k_u)\) corresponding to link \((k, u)\). Then, problem \(P_{\text{PFPCM}}\) can be approximated by the following problem

\[
\min_{\{v^k_u\}, p} \sum_{k \in K} \sum_{u \in L} p^k_u + q \sum_{k \in K} \sum_{u \in L} f_{\text{apx}}^{k,u}(p^k_u) R^k_u \quad \text{min} \quad \mathbf{x} \left(\nabla g(\mathbf{x}) \right) s.t. \mathbf{x} \in \mathcal{F}, \quad \mathbf{x} \in \mathcal{F},
\]

The objective function of this approximated problem is concave and the feasible region determined by all the constraints is convex. This problem is of the following general form

\[
\min g(\mathbf{x}) \quad \text{s.t.} \quad \mathbf{x} \in \mathcal{F}, \quad \mathbf{x} \in \mathcal{F},
\]

where \(g(\mathbf{x})\) is concave with respect to \(\mathbf{x}\) and \(\mathcal{F}\) is the corresponding feasible region. This problem can be solved by the standard gradient method as follows. We start with an initial solution \(\mathbf{x}^{(0)} \in \mathcal{F}\) and then iteratively update its solution as

\[
\mathbf{x}^{(n+1)} = \arg \min_{\mathbf{x}} g(\mathbf{x}) + \nabla g(\mathbf{x})(\mathbf{x} - \mathbf{x}^{(n)}) \quad \text{s.t.} \quad \mathbf{x} \in \mathcal{F}.
\]

In particular, \(\mathbf{x}^{(n+1)}\) needs to be determined from the following problem

\[
\min \mathbf{x} \left(\nabla g(\mathbf{x})\right) \mathbf{x} \quad \text{s.t.} \quad \mathbf{x} \in \mathcal{F}.
\]

Return to our problem and let \(x\) represent the precoding vectors and \(g(\mathbf{x})\) denote the objective function of problem (14). Then, we have \(\nabla g(\mathbf{x}) = \sum_{(k, u) \in L} (1 + q f_{\text{apx}}^{k,u}(p^k_u) R^k_u) p^k_u\). By applying the gradient method, we can solve problem (14) by iteratively solving the following problem until convergence

\[
\min_{\{v^k_u\}, p} \sum_{k \in K} \sum_{u \in L} \alpha^{k,u}(\mathbf{x}) v^k_u v^k_u \quad \text{s.t.} \quad \mathbf{x} \left(\nabla g(\mathbf{x})\right) \mathbf{x} \quad \text{s.t.} \quad \mathbf{x} \in \mathcal{F}.
\]
Algorithm 2 SDP-BASED ALGORITHM FOR PFCPM PROBLEM

1: Initialization: Set \( n = 0 \), and \( \alpha_u^{k(0)} = 1 \) for all RRH-user links \((k, u)\).
2: Iteration \( n \):
   a. Solve problem (18) with \( \alpha_u^{k(n-1)} \) to obtain \( \{p_u^{(n)}\} \) and \( \{v_u^{(n)}\} \).
   b. Update \( \alpha_u^{k(n)} \) as in (19).
3: Set \( n := n + 1 \) and go back to Step 2 until convergence.

where
\[
\alpha_u^{k(n)} = 1 + q \nabla f_{\text{apx}}^{(k,u)} (p_u^{k}) R_u^{k,fh}.
\]

Problem (18) is a weighted sum-power minimization problem, which can be transformed into the convex semi-definite program (SDP) as presented in Appendix A.

3) Algorithm Design: The algorithm to solve (14) is given in Algorithm 2. We have the following proposition which states the convergence property of Algorithm 2.

**Proposition 2.** Algorithm 2 converges to a local optimal solution of problem (14).

**Proof.** The proof is given in Appendix C.

Algorithm 1, which is proposed to solve problem \( \mathcal{P}_{\text{FCPM}} \), is based on the solution of problem \( \mathcal{P}_{\text{PFCPM}} \), which can be obtained by using Algorithm 2.

**B. Iterative Linear-Relaxed Algorithm**

In this section, we propose an iterative linear-relaxed algorithm to directly deal with the step-function fronthaul capacity constraint. Toward this end, we first propose to approximate the step-function constraint by an approximation function. By doing so, the non-continuous constraint with step functions becomes a continuous but still non-convex one. To convexify the obtained problem, the non-convex approximated constraint function is further relaxed to a linear form by using the concave duality method [32]. The linearized-relaxed constraint function can be made sufficiently close to the original non-convex function by iteratively updating its parameters. First, problem \( \mathcal{P}_{\text{FCPM}} \) can be approximated by the following problem

\[
\min_{\{v_u\}} \|p\|_1 \quad \text{s. t. constraints (1), (4), (5), (8),}
\]

\[
\sum_{k \in K \cup u \in U} f_{\text{apx}}^{(k,u)} (p_u^{k}) R_u^{k,fh} \leq C. \tag{21}
\]

As mentioned above, the function \( f_{\text{apx}}^{(k,u)} (p_u^{k}) \) is concave with respect to \( p_u^{k} \); hence, the constraint (21) is indeed non-convex. Hence, we approximate it by the corresponding linear form based on the duality properties of conjugate of convex functions [32] as follows. First, it can be verified that the function \( f_{\text{apx}}^{(k,u)} (p_u^{k}) \) can be rewritten by using its concave duality as

\[
f_{\text{apx}}^{(k,u)} (p_u^{k}) = \inf_{z_u^{k}} \left[ z_u^{k} p_u^{k} - f_{\text{apx}}^{(k,u)*} (z_u^{k}) \right], \tag{22}
\]

where \( f_{\text{apx}}^{(k,u)*} (z) \) is the conjugate function of \( f_{\text{apx}}^{(k,u)} (w) \), which can be expressed as

\[
f_{\text{apx}}^{(k,u)*} (z) = \inf_w \left[ z w - f_{\text{apx}}^{(k,u)} (w) \right]. \tag{23}
\]

According to [32], function \( f_{\text{apx}}^{(k,u)*} (z) \) can be determined by the optimal value of \( w \) obtained from the right hand side of (23) for a given \( z \). After substituting the results of (23) into (22), it can be verified that the optimization problem in the right hand side of (22) achieves its minimum at

\[
\hat{z}_u^{k} = \nabla f_{\text{apx}}^{(k,u)} (w)|_{w=p_u^{k}}, \tag{24}
\]

With the representation of \( f_{\text{apx}}^{(k,u)*} (z) \) as in (22), the constraints (9) can be rewritten in a linear form for a given \( \hat{z}_u^{k} \) as

\[
\sum_{k \in K \cup u \in U} \hat{z}_u^{k} R_u^{k,fh} p_u^{k} \leq C + \sum_{k \in K \cup u \in U} R_u^{k,fh} f_{\text{apx}}^{(k,u)*} (\hat{z}_u^{k}). \tag{25}
\]

In summary, for a given value of \( \hat{z}_u^{k} \), the problem (20)-(21) can be reformulated to

\[
\min_{\{v_u\}} \sum_{k \in K \cup u \in U} v_u^{k H} v_u^{k} \quad \text{s. t. constraints (4), (5), (8),}
\]

\[
\sum_{k \in K \cup u \in U} \hat{z}_u^{k} R_u^{k,fh} v_u^{k H} v_u^{k} \leq C + \sum_{k \in K \cup u \in U} R_u^{k,fh} f_{\text{apx}}^{(k,u)*} (\hat{z}_u^{k}). \tag{27}
\]

Now problem (26)-(27) is the well-known SPMP, which can be solved by transforming it into the SDP, which is described in Appendix A where the additional constraint (27) can be rewritten in (55). In summary, we can fulfill our design objectives by updating \( \{\hat{z}_u^{k}\} \) iteratively based on which we repeatedly solve the precoding problem (26)-(27).

This complete procedure is described in Algorithm 3 whose properties are stated in the following proposition.

**Proposition 3.** Algorithm 3 has the following properties

1) If the FCPM problem is feasible, Algorithm 3 converges.
2) The feasible solution achieved by Algorithm 3 at convergence satisfies all constraints of problem (20)-(21).

**Proof.** The proof is given in Appendix D.

**Remark 3.** Some careful study of \( \hat{z}_u^{k} \) given in (24) yields \( f_{\text{apx}}^{(k,u)} (p_u^{k}) = \hat{z}_u^{k} p_u^{k} - f_{\text{apx}}^{(k,u)*} (\hat{z}_u^{k}) \), which can be considered as the first-order approximation (first-order Taylor expansion) of \( f_{\text{apx}}^{(k,u)} (w) \) at \( w = p_u^{k} \). In our paper, we prefer using the conjugate function concept in approximating the conjugate function. This is because the property of the conjugate function, i.e.,
satisfies $\Gamma$ close to one for large power values so that it well approximates that this adjustment only results in tolerable performance degradation in the next subsection.

C. Adjusting Precoding and Power Solution

After running Algorithms 1 and 3, the obtained solution may have several small but non-zero power elements in the power vector $p^*$. Since the approximation function is smooth, there may be significant difference between $C(p^*)$ and $\sum_{k \in \mathcal{K}} \sum_{u \in \mathcal{M}} p_{k,u} f_{\text{apx}}^{(k,u)}(p_{k,u}^*)$. To address this problem, we force the power value and precoding vector to zero for any link $(k, u)$ as follows:

$$p_{k,u}^* = 0 \text{ if } f_{\text{apx}}^{(k,u)}(p_{k,u}^*) < 1/2. \quad (28)$$

We will show how to design the approximation function so that this adjustment only results in tolerable performance degradation in the next subsection.

D. Design of Approximation Function

This subsection discusses the design of an approximation function that is employed to approximate the step function in the fronthaul capacity constraint. Let us denote $p^*$ as the transmission vector achieved by any of our proposed algorithms at convergence. It can be verified that we have $\sum_{k \in \mathcal{K}} \sum_{u \in \mathcal{M}} R_{k,u}^{\text{fh}} f_{\text{apx}}^{(k,u)}(p_{k,u}^*) = C$ and the SINR of any user $u$ satisfies $\Gamma_u^* = \bar{\gamma}_u$.

First, we want the value of the approximation function to be close to one for large power values so that it well approximates the step function. Specifically, it is required that

$$f_{\text{apx}}^{(k,u)}(p_{k,u}^*) = 1. \quad (29)$$

In addition, we would like the adjusting procedure described in the previous subsection results in the deviation of at most $\epsilon$ for the achieved SINR of any user. Let $\Gamma_u^*|p_{k,u}^*=0$ denote the SINR achieved by user $u$ after we apply the adjustment procedure given in (28) for the obtained power vector $p^*$. Then, the results in the following proposition provide the guideline to achieve this design goal.

Proposition 4. If the approximation concave function satisfies the following condition

$$f_{\text{apx}}^{(k,u)}(a \beta_u^k) \geq 1/2, \quad (30)$$

where $\beta_u^k = \bar{\gamma}_u \sigma^2 / |h_{k,u}|^2$, then we have

$$\bar{\gamma}_u - \Gamma_u^*|p_{k,u}^*=0 < \epsilon. \quad (31)$$

Proof. The proof is given in Appendix E.

We provide an example of an exponential approximation function and the required conditions on its parameters in Table 1. Note that other choice of the approximation functions is possible as long as it satisfies the conditions stated in Proposition 4.

E. Complexity Analysis

The complexity of the exhaustive search and our proposed algorithms are now investigated based on the number of required computations. As can be observed, all these algorithms require us to solve SDMPs several times (i.e., $P_a$ for exhaustive search algorithm, (18) for the pricing-based algorithm, and (26) for the linear-relaxed algorithm) by transferring them into the SDP problems as described in Appendix A. Hence, we first study the complexity of the SDP program corresponding to each algorithm. We assume that all RRHs are equipped the same number of antennas $N$ and we consider the worst case where each UE can be served by all RRHs in the network. Then the numbers of variables of all SDP problems are the same, which is equal to $MNK$. On the other hand, the numbers of constraints of $(P_a)$ and (18) are $M + K$ while the corresponding number of (26) is $M + K + 1$. As given in [33], the computational complexity involved in solving the SDP is $O(\max(n,m)^{n/2} \log(\zeta^{-1}))$ where $n$ is the number of variables, $m$ is the number of constraints, and $\zeta$ represents the solution accuracy. In practice, the number of users is greater than that of RRHs and they are larger than 1, i.e., $M > K > 1$; hence, we have $MNK > M + K + 1$. Thus, we can express the complexity of solving problem $(P_a)$, (18) and (26) as

$$X_{\text{SDP}} = O\left((M^4.5) \log(\zeta^{-1})\right), \quad (32)$$

where $\Pi = MNK$. The complexity of the exhaustive search algorithm and our proposed algorithms can be calculated based on the number of iterations and $X_{\text{SDP}}$ as follows. First, let us define $R_{\text{min}}^{\text{fh}} = \min_{u \in \mathcal{U}} R_{k,u}^{\text{fh}}$ and $C = C/R_{\text{min}}^{\text{fh}}$. Then, the number of possible $a$ (i.e., the number of elements of set $S_a$) is upper bounded by $(MK/C)$. Hence, the complexity of the exhaustive search method can be expressed as

$$X_{\text{ech}} = \left(\frac{MK}{C}\right) \times X_{\text{SDP}} = O\left(\left(\frac{MK}{C}\right)^{2^5} \log(\zeta^{-1})\right). \quad (33)$$

We now quantify the complexity of solving FCPM problem using Algorithm 2, which is adopted in Algorithm 1. Note that in each iteration of Algorithm 2, problem (18) is solved with certain values of $\{a^k_u\}$ and $q$. For a given value of $q$, the number of iterations for solving PFCPM problem is $O(\zeta^{-2})$ because the gradient method is applied [42], where $\zeta$ represents the solution accuracy of Algorithm 2. In addition, using the bisection searching method, the value of $q$ is typically determined after $O(\log(\bar{\gamma}/\zeta_1^{-1}))$ searching steps where $\zeta_1$ denotes the solution accuracy of Algorithm 1. Hence, the complexity of Algorithm 1 can be calculated as

$$X_{\text{PBA}} = O\left(\zeta^{-2}\right) \times O\left(\log(\bar{\gamma}/\zeta_1)\right) \times X_{\text{SDP}} = O\left((M^4.5) \zeta^{-2} \log(\zeta^{-1})\right). \quad (34)$$

Finally, let $I_{\text{LRA}}$ be the number of iterations required in Algorithm 3 to solve the FCPM problem, the complexity of the Algorithm 3 can be given as

$$X_{\text{LRA}} = I_{\text{LRA}} \times X_{\text{SDP}} = O\left(I_{\text{LRA}} (M^4.5) \log(\zeta^{-1})\right). \quad (35)$$

As illustrated in the numerical results, Algorithm 3 converges very fast around 10 iterations for the small system and
30 iterations for the large system. Hence, Algorithm 3 is less complex than Algorithm 1. Moreover, this complexity study also shows that the complexities of our proposed algorithms are much lower than that of the exhaustive searching method.

**F. Existing Algorithms**

We present two existing algorithms in [23] and [25] to evaluate the relative performance of our proposed algorithms in Section V. These works also attempt to determine the set of RRHs-user links for each user even through their considered problems are different from ours. Therefore, these existing algorithms are modified so that they can be applied to solve our considered problem. This is described in the following.

1) _Zhao, Quek, and Lei (ZQL) algorithm [23]:_ We first describe the greedy algorithm proposed by Zhao, Quek, and Lei (ZQL), named as _Iterative Link Removal algorithm_ in [23]. In this work, the authors aim to minimize the number of active BS-user links (i.e., fronthaul capacity minimization) subject to the constraints on BSs’ maximum transmission power and users’ target SINRs. This greedy iterative algorithm works as follows. In each iteration, the power-minimization precoding problem with a specific set of active BS-user links is solved where the authors allow all possible BS-user links initially. If this problem is feasible (i.e., all power and QoS constraints can be supported) then the active BS-user links are sorted in the increasing order of their required transmission powers. Then, the set of removed BS-user links is updated before the whole procedure is repeated in the next iteration.

If the power-minimization precoding problem is not feasible in a particular iteration, then the number of removed BS-user links is reduced compared to that in the previous iteration. Otherwise, we increase the number of removed BS-user links. These updates for the number of removed BS-user links follow the bisection method. This iterative procedure is repeated until the largest number of removed BS-user links can be determined while all constraints can still be maintained.

This greedy link removal principle can be applied to solve our problem as follows. We initially solve the precoding problem for power minimization where all possible RRH-user links are allowed. Then, the required powers of all RRH-user links are sorted in the increasing order based on which we remove the minimum number of links with lowest powers so as to maintain the fronthaul capacity constraint. Finally, we solve the precoding problem again to determine the precoding and power allocation solution.

2) _Dai and Yu (DY) algorithm [25]:_ The second algorithm is proposed by Dai and Yu (DY) [25] where the authors consider the sum-rate maximization problem subject to the constraints on RRHs’ transmission power and fronthaul capacity similar to (38). The main idea of this algorithm is to approximate the step-function in the fronthaul constraint by a simple function and solve the corresponding optimization problem iteratively. Specifically, the fronthaul capacity constraint is approximated as follows [25]:

\[
\sum_{k \in K} \sum_{u \in \mathcal{U}} \beta_{u}^{k} p_{u}^{k} \leq C,
\]

where \(\beta_{u}^{k}\) is a parameter associated with the link between RRH \(k\) and user \(u\), which is updated iteratively as

\[
\beta_{u}^{k} = \frac{1}{p_{u}^{k} + \tau},
\]

where \(\tau\) is a small number.

This approximation can be employed to solve our problem by iteratively solving the problem (26)-(27) where the fronthaul capacity constraint is approximated by (36). The limitation of this approximation is that convergence cannot be established. In addition, we will show later in Section V that our proposed algorithms achieve better performance than this algorithm in all investigated simulation settings.

**IV. FURTHER EXTENSION**

**A. Individual Fronthaul Capacity Constraints**

In this section, we discuss the extension of the considered CoMP transmission design where there are multiple individual fronthaul capacity constraints. In particular, each of these constraints captures the limited capacity of one particular fronthaul link between the CPC and the corresponding RRH. In this scenario, we have to replace the sum fronthaul capacity constraint (9) with the following set of constraints

\[
G_{k}(\mathbf{p}^{k}) = \sum_{u \in \mathcal{M}} p_{u}^{k} \delta_{u}(p_{u}^{k}) \leq C_{k}, \quad \forall k \in \mathcal{K},
\]

where \(C_{k}\) denotes the capacity limit corresponding to the fronthaul link of RRH \(k\). Then, we have the following individual fronthaul constraint power minimization (IFCPM) problem

\[
\min_{\{\nu_{k}^{k}\}, \mathbf{p}} \|\mathbf{p}\|_1 \quad \text{s. t. constraints } (1), (4), (5), (8), (38).
\]

Obviously, problem \(\mathcal{P}_{\text{IFCPM}}\) is more challenging to address than problem \(\mathcal{P}_{\text{FCPM}}\). However, we show in the following that the same design principles adopted in the previous section can be employed to develop low-complexity algorithms in this scenario as well.

1) _Pricing-Based Algorithm:_ To address multiple fronthaul capacity constraints in this case, we have to consider the pricing problem with multiple corresponding pricing parameters \(q_{k}\) whose objective is given as follows:

\[
\min_{\{\nu_{k}^{k}\}, \mathbf{p}} \|\mathbf{p}\|_1 + \sum_{k \in \mathcal{K}} q_{k} G_{k}(\mathbf{p}^{k}).
\]

For given pricing parameters \(q_{k}, k \in \mathcal{K}\), the pricing problem can also be transformed into the convex SDP form based...
on which we can determine the precoding vectors. The key challenge is how to iteratively adjust the pricing parameters \( q_k \) to satisfy all fronthaul capacity constraints. Such procedure has been presented in our previous conference work \[29\], which is omitted here due to the space constraint.

2) Iterative Linear-Relaxed Algorithm: We can apply the same linearization technique to the sum fronthaul capacity constraint in Section III-B to deal with each fronthaul capacity constraint in (38) for problem \( P_{IFCPM} \). In particular, these constraints can be relaxed into the following form

\[
\sum_{u \in U} z_k R_{u,k} \text{fh \text{,fh}} v^H_k v_k \leq C_k + \sum_{u \in U} R_{u,k} \text{apx}(k,u) z_k, \quad \forall k \in K. \tag{41}
\]

Then, these constraints can be transformed into the convex SDP form as in \( (56) \).

B. MIMO Systems with Multi-Stream Communications

We now discuss how our proposed algorithms for MISO systems can be extended for the MIMO systems where multiple data streams can be transmitted to each user. Let us consider a multi-stream communication setting where user \( u \) is equipped with \( T_u \) antennas and \( D_u \) data streams are transmitted to each user \( u \) where \( D_u \leq T_u \leq \min_{u \in K} N_u \). Denote \( x_u = [x_{u,1}, x_{u,2}, \ldots, x_{u,D_u}]^T \in \mathbb{C}^{T_u \times 1} \) as the vector describing \( D_u \) data streams for user \( u \) where \( \mathbb{E}\{x_u x_u^H\} = I_{D_u \times D_u} \). Moreover, let \( V_u = [v_{u,1}^H, v_{u,2}^H, \ldots, v_{u,D_u}^H] \in \mathbb{C}^{N_u \times D_u} \) denote the precoding matrix at RRH \( k \) corresponding to the signal transmitted to user \( u \) as in \[40\]. \( U_u = [u_{u,1}, u_{u,2}, \ldots, u_{u,D_u}] \in \mathbb{C}^{T_u \times D_u} \) be the decoding matrix of user \( u \) and \( H_u \in \mathbb{C}^{T_u \times N_u} \) be the channel matrix between RRH \( k \) and user \( u \). Then, the baseband signal \( y_u \) received at user \( u \) can be written as

\[
y_u = U_u^H \left( \sum_{u \in K} \sum_{k \in K} H_u^k v^H_k x_t + \Xi_u \right), \tag{42}
\]

where \( \Xi_u \in \mathbb{C}^{T_u \times 1} \) denotes the additive noise vector and \( \mathbb{E}\{\Xi_u \Xi_u^H\} = \sigma^2 I_{D_u \times D_u} \). Then, the received baseband signal for stream \( m \) of user \( u \) can be expressed as

\[
y_{u,m} = \sum_{k \in K} u_{u,m}^H h_{u,m}^k v^H_k x_t + \sum_{i=1}^{M} \sum_{\lambda \in \mathcal{L}_i} u_{u,m}^H h_{u,m}^k v^H_{i,t} r_{i,t} + u_{u,m}^H \Xi_u. \tag{43}
\]

Moreover, the SINR of stream \( m \) of user \( u \) can be given as

\[
\Gamma_{u,m} = \frac{\left| \sum_{k \in K} u_{u,m}^H h_{u,m}^k v^H_{k,m} \right|^2}{\sum_{(i,t) \neq (u,m)} \left| \sum_{\lambda \in \mathcal{L}_i} u_{u,m}^H h_{u,m}^k v^H_{i,t} r_{i,t} \right|^2 + \sigma^2 |u_{u,m}|^2}. \tag{44}
\]

Assume that each data stream \( m \) of every user \( u \) has a QoS requirement, which is represented by target SINR \( \gamma_{u,m} \). Our design problem for the MIMO system with multi-stream communications, \( (P_{MIMO}) \), can be written as

\[
\min_{\{V_u\},\{U_u\}} \sum_{u \in U} \text{Tr} (V_u^H V_u) \tag{45}
\]

s. t. \( \sum_{u \in U} \text{Tr} (V_u^H V_u) \leq P_k, \quad \forall k, \tag{46} \)

\[
\Gamma_{u,m} \geq \gamma_{u,m}, \quad \forall (u,m), \tag{47} \]

\[
\text{Tr} (V_u^H V_u) = 0 \text{ if } (k,u) \notin \mathcal{L}, \tag{48} \]

\[
\sum_{\forall (u,m) \in \mathcal{L}} \delta(V_u^H V_u) R_{u,m}^k \text{fh} \leq C, \tag{49} \]

where these constraints capture the power limitation of RRHs, the QoS requirement of each data stream, the clustering constraint, and the limited fronthaul capacity, respectively. Here, \( R_{u,m}^k \text{fh} \) represents the required fronthaul capacity of RRH \( k \) for transmitting the precoding vector and data stream \( m \) of user \( u \). As described in \[41\], for a given fixed precoding matrix, the optimal decoding matrix based on the MMSE criterion can be expressed as

\[
U_u^* = \left( \sum_{\forall (u,m) \in \mathcal{L}} \sum_{i \in \mathcal{L}_i} H_u^i v^H_i v^H_{i,t} H_{u,m}^H + \sigma^2 I_{D_u \times D_u} \right)^{-1} H_u^k v^H_k. \tag{50}
\]

Then, if \( U_u \) is given, we can treat each user \( u \) as \( D_u \) virtual users \( \{u_1, u_2, \ldots, u_{D_u}\} \). Specifically, each virtual user \( u_m \) \((m \in \{1, 2, \ldots, D_u\})\) receives a single data stream represented by data symbol \( x_{u,m} \), the virtual channel vector between RRH \( k \) and user \( u_m \) can be expressed as \( h_{u,m}^k = H_u^k u_{u,m} \), and the power noise \( \sigma^2_{u,m} = \sigma^2 |u_{u,m}|^2 \). Therefore, the multi-stream design problem can be reformulated by the corresponding virtual single-stream one. Consequently, our proposed algorithms for the single-stream MISO setting can be applied to determine the precoding matrices for this multi-stream MIMO system. Based on these results, we can easily develop an iterative algorithm, which is similar to the one in \[41\], to solve the multi-stream problem where we alternatively determine the precoding matrices and decoding matrices in each iteration.

V. NUMERICAL RESULTS

We present numerical results to illustrate the performance achieved by our proposed algorithms. To obtain all numerical results for our proposed algorithms, we employ the exponential approximation function given in Table. I. To demonstrate the
effectiveness of our design, we consider a small network simulation setting as illustrated in Fig. 2a, which allows us to obtain the global optimal solution based on exhaustive search. We then further study the network performance for a larger network setting shown in Fig. 2b. For ease of exposition, we will present all results using normalized fronthaul capacity, which is defined as $C = C / P_{\text{fh}}^{\text{min}}$, where $P_{\text{fh}}^{\text{min}} = \min_{u \in U} R_k^{\text{fh}}$. Furthermore, the initial solution for our iterative linear-relaxed algorithm and DY algorithm [25] is obtained by running Algorithm 2 with the pricing parameter $\bar{q}$. Unless stated otherwise, the following parameter and simulation setup are adopted for both network settings. The channel gains are generated by considering both Rayleigh fading and path loss which is modeled as $L_u^k = 36.8 \log_{10}(d_u^k) + 43.8 + 20 \log_{10}(\frac{f_c}{25})$ where $d_u^k$ is the distance from user $u$ to RRH $k$; $f_c = 2.5 GHz$. The noise power is set equal to $\sigma^2 = 10^{-13} W$. We set other parameters as follows: $\epsilon = 10^{-6}$, $\tau = 10^{-8}$, RRH power $P_k = 3 W$ for all $k \in K$, the number of antennas of each RRH equal to 4 except for the results in Fig. 6. We denote our proposed algorithms and two existing algorithms as “Pricing-Based Alg.”, “Iterative Linear-Relaxed Alg.”, “ZQL Alg.” [23], and “DY Alg.” [25], respectively in relevant figures.

### A. Small Network Simulation Setting

We consider three RRHs in this setting where the distance between their centers is equal to 500 m. Users are randomly placed inside a circle at the center of three RRHs whose radius is 125 m. First, we examine the convergence of our proposed algorithms and DY algorithm in Fig. 3. Three different curves represent the variations of total transmission powers due to the pricing-based algorithm, the iterative linear-relaxed algorithm and DY algorithm, respectively. To obtain these simulation results, we set the number of users equal to 7 ($M = 7$), and user target SINR $\gamma_u = 0 dB$ for all $u \in \mathcal{M}$. It can be observed that all algorithms converge even though the iterative linear-relaxed algorithm is fastest and the pricing-based algorithm is slowest but it achieves the lowest transmission power. This figure also illustrates that the DY algorithm converges after 20 iterations; however, the transmission power achieved by this algorithm is much higher than those achieved by ours.

In Fig. 4, we show total transmission powers of all RRHs achieved by the exhaustive searching method, our proposed algorithms, and two reference algorithms, versus the number of users where the user target SINR is $\gamma_u = 0 dB$. As can be seen, our proposed algorithms result in lower total transmission power compared to DY and ZQL algorithms. Moreover, the pricing-based algorithm is slightly better than the iterative linear-relaxed algorithm, and both proposed algorithms require marginally higher total transmission power than that due to the optimal exhaustive search algorithm. In addition, the DY algorithm outperforms the ZQL algorithm but these existing algorithms demand considerably higher powers compared to our algorithms. Also, this figure shows that the total transmission power increases as the number of users becomes larger under all algorithms as expected.

Fig. 5 and Fig. 6 illustrates the variations of total transmission power versus user target SINR and the number of antennas per RRH for $M = 7$, respectively. The target SINR of all users for the scheme in Fig. 6 is set as $\gamma_u = 0 dB$. As expected, larger power is needed as users require a higher target SINR, and larger number of equipped antennas results in reduction of total transmission power due to the increasing network degrees of freedom. In addition, our proposed algorithms can achieve the total transmission powers which are close to that obtained by the exhaustive search method. Moreover, as can be observed, these figures also confirm the superiority of the proposed algorithms compared to the reference algorithms. Once again, the pricing-based algorithm slightly outperforms the iterative linear-relaxed algorithm.
B. Large Network Simulation Setting

We now study the performance of the proposed algorithms for the large network simulation setting where there are 10 hexagonal cells ($K = 10$) and the distance between the centers of two nearest RRHs is 500 m. In this setting, three users are randomly placed inside each cell so that the distance between each of them and their nearest RRH is either 250 m or 125 m. Overall, we generate 30 users ($M = 30$) in this network and we set $\bar{\gamma}_u = 0$ dB for all users except the simulation in Fig. 9.

Fig. 7 illustrates the convergence of two proposed algorithms and DY algorithm where it confirms that our proposed algorithms also perform as expected in this large network setting. Moreover, the pricing-based algorithm requires more convergence time compared to the iterative linear-relaxed algorithm and DY algorithm even through the former achieves smaller transmission power than the later. Once again, the iterative linear-relaxed algorithm converges faster than DY algorithm.

Figs. 8, 9 show the total transmission powers versus the normalized fronthaul capacity and users’ target SINR, respectively. Our proposed algorithms again outperform the other existing algorithms. The iterative linear-relaxed algorithm results in the total transmission power which is slightly higher than that due to the pricing-based algorithm. Moreover, as can be seen from Fig. 8, the performance gap between these algorithms are more significant if the available fronthaul capacity is smaller. Furthermore, the three algorithms except ZQL algorithm achieve similar performance for sufficiently large fronthaul capacity or small target SINR values.

In Fig. 10, we present the variations of total transmission power versus user target SINR in dB.
Again, the individual normalized fronthaul capacity is defined 1 and 2, which is denoted as normalized capacity of fronthaul links corresponding RRHs.

As can be seen, the larger cluster size results in the lower total transmission power. However, total transmission powers achieved by all algorithms become flat as the cluster size is sufficiently large. These results imply that activating weak links between users and RRHs does not significantly improve the network performance. This figure again confirms that our proposed algorithms still work well for the MIMO stream and also achieve better solution than that of the algorithm in literatures. Interestingly, the higher number of streams per user requires the higher transmission power of all RRHs.

C. Individual Fronthaul Capacity Constraints

Fig. 11 shows variations of total transmission powers achieved by our proposed algorithms and two reference algorithms as there are multiple individual fronthaul capacity constraints. In this simulation, we keep the normalized fronthaul capacity \( C_k = 8 \) for all \( k > 2 \) while varying the normalized capacity of fronthaul links corresponding RRHs 1 and 2, which is denoted as \( \bar{C}_{1-2} \) (i.e., \( \bar{C}_1 = \bar{C}_2 = \bar{C}_{1-2} \)). Again, the individual normalized fronthaul capacity is defined as \( \bar{C}_k = C_k / P_{\text{th}} \). In fact, if we set \( \bar{C}_{1-2} = 0 \), then RRHs 1 and 2 are turned off, which cannot serve any user in the network. As can be observed, the total transmission power decreases with the increase of \( \bar{C}_{1-2} \), which shows a similar trend as in Fig. 8. Interestingly, all users in cells 1 and 2 can still be supported at their target SINR by running pricing-based, iterative linear-relaxed and DY algorithms even when RRHs 1 and 2 are turned off, which is not the case with the ZQL algorithm. Overall, our proposed algorithms still outperform the two existing algorithms.

D. MIMO Systems with Multi-Stream Communications

For this simulation, we consider the large network but we allocate only 2 users in each cell to ensure the feasibility of the network. Each RRH is equipped 8 antennas and each user has 4 antennas. The total normalized fronthaul capacity is set at 100, and the target SINR for each stream is 0 dB. Fig. 12 illustrates the total transmission power of all RRHs versus the number of data streams for each users. As can be seen, the proposed algorithms still work well for the MIMO stream and also achieve better solution than that of the algorithm in literatures. Interestingly, the higher number of streams per user requires the higher transmission power of all RRHs.

VI. CONCLUSION

We have proposed efficient and low-complexity algorithms to solve the downlink joint transmission problem in Cloud-RAN that aims to minimize the total transmission power subject to constraints on transmission powers, fronthaul capacity, and users’ QoS. We have considered both scenarios with sum and individual fronthaul capacity constraints. Numerical results have illustrated the efficacy of our proposed algorithms and the impacts of different parameters on the network performance. In particular, the pricing-based and iterative linear-relaxed algorithms achieve the performance very close to that due to the optimal exhaustive search. In addition, our proposed algorithms significantly outperform two existing algorithms proposed in [23], [25] in all investigated scenarios. There are
still several interesting directions for future study. First, joint design and optimization of CoMP techniques and fronthaul signal compression is an interesting problem. Furthermore, consideration of CoMP design, CSI estimation, and feedback deserves further efforts.

**Appendix A**

**Weighted Sum-Power Minimization Solution**

Denote $\mathcal{K}_u$ as the set of RRHs allowed to serve user $u$, i.e., $\mathcal{K}_u = \{k | (k, u) \in \mathcal{L}\}$. Let $\mathbf{v}_u$ denote the precoding solution over all RRHs in $\mathcal{K}_u$, which is defined as $\mathbf{v}_u = [v_{u1}^T, v_{u2}^T, \ldots, v_{um}^T]^T$ where $\{u_1, \ldots, u_m\} = \mathcal{K}_u$ and $a_u = |\mathcal{K}_u|$. So, we have $\mathbf{v}_u \in \mathbb{C}^{N_u \times 1}$ where $N_u = \sum_{k \in \mathcal{K}_u} N_k$.

Here, we are interested in determining $\mathbf{v}_u$ because we have $v_{ui} = 0$ for all $i \notin \mathcal{K}_u$ (i.e., the precoding vector of any RRH that does not serve the underlying user is equal to zero).

Let us define $W_u = v_u v_u^H$, we have $W_u \in \mathbb{C}^{N_u \times N_u}$. It is positive semi-definite ($W_u \geq 0$) and has rank one because it is generated from vector $\mathbf{v}_u$. We also define the channel vector $h_{u, i} = [h_{u1}^T, h_{u2}^T, \ldots, h_{um}^T]^T$ and $h_{u, i} = h_{u1} h_{u1}^H$ for all $u, i \in \mathcal{U}$. Then, the SINR constraint for user $u$ in (4), and the power constraint for RRHs can be rewritten as

$$Tr(H_{a,i} W_u) - g_u \sum_{i \in \mathcal{U}/u} Tr(H_{a,i} W_i) \geq g_u n^2, \forall u \in \mathcal{U}, \quad (51)$$

$$\sum_{u \in \mathcal{U}} Tr(E_{u} W_i) \leq P_k, \forall k \in \mathcal{K}, \quad (52)$$

where $E_{u} = \text{diag}(0_{N_u \times 1}, \ldots, 1_{N_u \times 1}, \ldots, 0_{N_{\text{equ}u \times 1}})$ if $u_i = k$. Therefore, the weighted sum-power minimization can be formulated as the following SDP problem

$$\min_{\{W_u\}_{u=1}^M} \sum_{u=1}^M Tr(F_u W_u)$$

s.t. constraints (51), (52),

$$W_u \geq 0, \text{rank}(W_u) = 1, \forall u, \quad (54)$$

where $F_u = \text{diag}(\alpha_{u1}^{(n)} 1_{N_u \times 1}, \ldots, \alpha_{um}^{(n)} 1_{N_u \times 1})$. This transformation reveals a special structure of the precoding design problem. Specifically, if we remove the rank-one constraints in (54) from (53) then the new problem is convex. In fact, this relaxed problem is the convex semi-definite program (SDP), which can be, therefore, solved easily by using standard tools such as CVX solver [31]. As given in Theorem 3.1 of [21] and Lemma 2 of [36], if (53) is feasible, then it has at least one solution where rank($W_u$) = 1, for all $u \in \mathcal{U}$.

Because the relaxed SDP problem is convex, $\mathbf{v}_u$ can be calculated as the eigenvector of $W_u$ if the optimum solution is unique. Such unique optimum solution satisfies the rank-one constraint. As discussed in [21, 36], the relaxed SDP may have more than one optimum solution, which means that the CVX solver cannot ensure to return the rank-one solution in general. However, this situation almost surely never happens in practice, except for cases where the channels from two groups are exactly symmetric. Nevertheless, if the algorithm does produce one of such solutions where $W_u$ does not have rank one, we can still obtain rank-one optimum solution from that solution by using the method described in Lemma 5 of [36], or by applying the solution method for solving the rank constrained problem presented in Algorithm 2 of [37], or by utilizing the best rank-one approximation based on the largest eigenvalue and the corresponding eigenvector as discussed in Section II of [33].

In addition, this SDP-based transformation can be applied to solve the problems (26)-(27) and (39) where the additional linear-relaxed fronthaul constraints (27) and (41) can also be rewritten respectively into the SDP-form as follows:

$$\sum_{u \in \mathcal{U}} R_{u1, u2}^k \text{tr}(Z_u W_u) \leq C + \sum_{k \in \mathcal{K}} \sum_{u \in \mathcal{U}} R_{u1, u2}^k f(k, u) \sigma(z_u^k), \quad (55)$$

and

$$\sum_{u \in \mathcal{U}} R_{u1, u2}^k \text{tr}(Z_u W_u) \leq C_k + \sum_{u \in \mathcal{U}} R_{u1, u2}^k f(k, u) \sigma(z_u^k), \quad (56)$$

where $Z_u = \text{diag}(z_{u1}^u 1_{N_u \times 1}, \ldots, z_{um}^u 1_{N_u \times 1})$ and $Z_k^u = \text{diag}(0_{N_u \times 1}, \ldots, z_{um}^u 1_{N_u \times 1}, \ldots, 0_{N_{\text{equ}u \times 1}})$ if $u_i = k$.

**Appendix B**

**Proof of Proposition 1**

**A. Proof of Statement 1**

Let us consider two values of the pricing parameter $q$ and $q'$ where $q' > q$. Let $(p, \{v_u^k\})$ and $(p', \{v_u'^k\})$ be the solutions of PFCPM problem with $q$ and $q'$, respectively. Then, we have

$$\sum_{(u, j) \in \mathcal{L}} p_i^u + q \sigma G_{PFCPM}(q) \leq \sum_{(u, j) \in \mathcal{L}} p_i^u + q \sigma G_{PFCPM}(q'), \quad (57)$$

$$\sum_{(u, j) \in \mathcal{L}} p_i^u + q' \sigma G_{PFCPM}(q') \leq \sum_{(u, j) \in \mathcal{L}} p_i^u + q' \sigma G_{PFCPM}(q). \quad (58)$$

After combining and simplifying these two inequalities, we have $(q' - q) \sigma G_{PFCPM}(q') \leq (q' - q) \sigma G_{PFCPM}(q)$. Therefore, we have finished the proof for the first statement.

**B. Proof of Statement 2**

We prove that for any $(p, \{v_u^k\})$ satisfying constraints (1), (4), (8), we always have $G(p) \geq G_{PFCPM}(q)$ if $q \geq \bar{q}$. Let $P_{\text{opt}}(q)$ be the total power of PFCPM problem corresponding to $q$. Because $(p, \{v_u^k\})$ satisfy constraints (1), (4), (8), we have

$$P_{\text{opt}}(q) + q \sigma G_{PFCPM}(q) \leq \sum_{(k, u) \in \mathcal{L}} p_i^u + q \sigma G(p), \quad (59)$$

$$\Rightarrow G_{PFCPM}(q) - G(p) \leq \frac{\sum_{(k, u) \in \mathcal{L}} p_i^u - P_{\text{opt}}(q)}{q} < \frac{\sum_{k \in \mathcal{K}} P_k}{q}. \quad (60)$$

Thus, we have $G_{PFCPM}(q) - G(p) < \sigma_{\text{min}}$ if $q \geq \bar{q}$. Based on the definition of $\sigma_{\text{min}}$, we must have that $G(p)$ cannot be smaller than $G_{PFCPM}(q)$.

**C. Proof of Statement 3**

From the proof of statement 2, we can see that there exists no $(p, \{v_u^k\})$ satisfying constraints (1), (8), (4) so that $G(p) \leq C < G_{PFCPM}(q)$. Hence, the last statement of Proposition 1 is proved.
APPENDIX C
PROOF OF PROPOSITION 2

To prove the convergence of Algorithm 2, we will prove that the value of the objective function of problem (14) (which is represented by \( g(x) \)) decreases after each step of Algorithm 2. For any vector \( x \) representing all precoding vectors and powers, the following inequality holds because of the concavity of function \( g(x) \)

\[
g(x) \geq g(x^{(n)}) + \nabla g(x^{(n)}) \left( x - x^{(n)} \right).
\]

(61)

In addition, the solution achieved in the \((n+1)\)th iteration is

\[
x^{(n+1)} = \arg \min \nabla g(x^{(n)}) x \text{ s.t. constraints } (4), (5), (8).
\]

Hence, we have \( \nabla g(x^{(n)}) x^{(n+1)} \leq \nabla g(x^{(n)}) x^{(n)} \). Substituting \( x^{(n+1)} \) into the inequality (61) yields

\[
g(x^{(n+1)}) \leq g(x^{(n)}) + \nabla g(x^{(n)}) \left( x^{(n+1)} - x^{(n)} \right) \leq g(x^{(n)}).
\]

(62)

Thus, the objective function of problem (14) corresponding to the solution in each iteration of Algorithm 2 is monotonically decreasing. Therefore, Algorithm 2 must converge to a local optimum point.

APPENDIX D
PROOF OF PROPOSITION 3

A. Proof of Statement 1

Denote \( \Omega_l \) as the optimum objective value of problem (26)-(27) in iteration \( l \), which is obtained after performing steps 8-12. We will prove that \( \Omega_l \) decreases over each iteration; hence, our proposed algorithm converges. Denote \( \mathcal{F}_l \) as the feasible set of (26)-(27) in iteration \( l \), which corresponds to the value of \( \{z_u^{(l)}\} \). Let us define \( \{p^{(l)}\}, \{v_u^{(l)}\} \) as the optimal solution of problem (26)-(27) corresponding to \( \{z_u^{(l)}\} \) as we run steps 8-12 in Algorithm 3. By setting \( \{z_u^{(l)}\} \) as in (24), we always have \( \{p^{(l)}\}, \{v_u^{(l)}\} \in \mathcal{F}_l \). Hence, we must have

\[
\Omega_l \geq \Omega_{l+1}, \quad \forall l > 0,
\]

(63)

which completes the proof.

B. Proof of Statement 2

Denote \( \mathcal{F} \) as the feasible set of problems (20)-(21). Because of (22), if \( \sum_{k \in \mathcal{K}} \sum_{u \in l} z_u^{(k,l+1)} P_u \leq C + \sum_{k \in \mathcal{K}} \sum_{u \in l} R_u^{(k,l)} f_{\text{apx}}^{(k,u)} (z_u^{(k)}) \), we have \( \sum_{k \in \mathcal{K}} \sum_{u \in l} R_u^{(k,l)} f_{\text{apx}}^{(k,u)} (z_u^{(k)}) \leq C \) for any value of \( \{z_u^{(k,l+1)}\} \). Therefore, we have \( \mathcal{F}_l \subseteq \mathcal{F} \) for any iteration \( l \), which means the optimal solution of problem (26)-(27) in any iteration \( l \) satisfies all constraints of problem (20)-(21). Hence, Algorithm 3 returns the solution that satisfies all constraints of problem (20)-(21).

APPENDIX E
PROOF OF PROPOSITION 4

Let \( p^* \) and \( \{v_u^{k_*}\} \) be the power vector and precoding vectors achieved after running our proposed algorithms. Because these results are obtained by solving a weighted sum-power minimization with SINR constraint for each user, we have

\[
\tilde{\gamma}_u = \left| \sum_{j \in \mathcal{K}} h_u^{H} v_j^* \right|^2 / \left( \sum_{j \in \mathcal{K}} h_u^{H} v_j^* \right)^2 + \sigma^2.
\]

(64)

Applying the triangle inequality yields

\[
\sum_{j \in \mathcal{K}} h_u^{H} v_j^* \left| \left| \sum_{j \in \mathcal{K}} h_u^{H} v_j^* \right| \right|^2 \leq \left| \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right|^2 + \sigma^2 \leq \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \left| \left| \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right| \right|^2 + \sigma^2.
\]

(65)

Now suppose that the power of user \( u \) and RRH \( k \) is forced to be zero (i.e., \( p_u^{k_*} = 0 \)), then its updated SINR becomes

\[
\Gamma_{u/p_u^{k_*}=0} = \left| \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right|^2 / \left( \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right)^2 + \sigma^2
\]

(66)

Consider the contribution of the underlying power \( p_u^{k_*} \), we have

\[
\left( \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right)^2 \leq \left( \sum_{j \in \mathcal{K}/u} h_u^{H} v_j^* \right)^2 \sigma^2 = \left| h_u^* \right|^2 p_u^{k_*} / \sigma^2.
\]

(67)

Combining all these results in (64)-(67) yields

\[
\tilde{\gamma}_u - \Gamma_{u/p_u^{k_*}=0} \leq \frac{\left| h_u^* \right|^2 p_u^{k_*}}{\tilde{\gamma}_u \sigma^2}.
\]

(68)

Because we have assumed that \( p_u^{k_*} \) is forced to be zero as in (28) and \( f_{\text{apx}}^{(k,u)}(x) \) is an increasing function, we have \( p_u^{k_*} < f_{\text{apx}}^{(k,u)}(x) \) for any \( x \). Using the inverse function of \( f_{\text{apx}}^{(k,u)}(x) \), the following inequality holds:

\[
\tilde{\gamma}_u - \Gamma_{u/p_u^{k_*}=0} \leq \frac{\left| h_u^* \right|^2 p_u^{k_*}}{\tilde{\gamma}_u \sigma^2} = \epsilon.
\]

(69)

This completes the proof of Proposition 4.

REFERENCES
[1] Cisco visual networking index: Global mobile data traffic forecast update, 2013–2018. White Paper, Feb. 2014.
[2] “Mobility Report,” Ericsson, Tech. Rep., Nov. 2013.
[3] E. Hossain, L. B. Le, and D. Niyato, Radio Resource Management in Multi-Tier Cellular Wireless Networks. New York, NY, USA: Wiley, 2013.
[4] N. Saquiuf, E. Hossain, Long B. Le, and D. I. Kim, “Interference management in OFDMA femtocell networks: Issues and approaches,” IEEE Wireless Commun., vol. 19, no. 3, pp. 86–95, Jun. 2012.

[5] L. B. Le, V. Lau, E. Jorswieck, A. Haghighat, D.-I. Kim, and T. Le-Ngoc, “Enabling 5G mobile wireless technologies,” EURASIP J. Wirel. Commun. Networking., 218, 2015.

[6] M. Sawahashi, Y. Kishiyama, A. Morimoto, D. Nishikawa, and M. Tanno, “Coordinated multipoint transmission/reception techniques for LTE-advanced [Coordinated and distributed MIMO],” IEEE Wireless Commun., vol. 17, no. 3, pp. 26–34, Jun. 2010.

[7] S.-H. Park, O. Simeone, O. Sahin and S. Shamai (Shitz), “Robust beamforming and user-centric clustering,” IEEE Trans. Wireless Commun., vol. 14, no. 1, pp. 230–241, Jan. 2015.

[8] Y. Shi, J. Zhang, and K. B. Letaief, “Group sparse beamforming for CoMP transmissions using mixed integer conic programming,” IEEE Trans. Signal Process., vol. 61, no. 16, pp. 3972–3987, Aug. 2013.

[9] B. Dai and W. Yu, “Sparse beamforming and user-centric clustering for downlink cloud radio access network,” in IEEE Access, vol. 2, no. 1, pp. 494–508, Jan. 2015.

[10] M. Bengtsson and B. Ottersten, “Optimal downlink beamforming using semidefinite programming,” IEEE Trans. Wireless Commun., vol. 13, no. 1, pp. 204–215, Jan. 2014.

[11] A. Lui and V. K. N. Lau, “Joint power and antenna selection optimization in large cloud radio access networks,” IEEE Trans. Signal Process., vol. 62, no. 5, pp. 1319–1328, Mar. 2014.

[12] Y. Shi, J. Zhang, and K. B. Letaief, “Group sparse beamforming for green Cloud-RAN,” IEEE Trans. Wireless Commun., vol. 13, pp. 2809–2823, May 2014.

[13] S. Luo, R. Zhang, and T. J. Lim, “Downlink and uplink energy minimization through user association and beamforming in cloud RAN,” IEEE Trans. Commun., vol. 61, no. 4, pp. 1340–1356, Apr. 2013.

[14] M. Bengtsson and B. Ottersten, “Optimal downlink beamforming using semidefinite optimization,” in Proc. Annual Allerton Conf. on Commun., Control and Computing, Monticello, NY, pp. 987–996, Sept. 1999.

[15] Z.-Q. Luo and W. Yu, “An introduction to convex optimization for communications and signal processing,” IEEE J. Sel. Areas Commun., vol. 24, no. 8, pp. 1426–1438, Aug. 2006.

[16] J. Zhao, T. Q. S. Quek, and Z. Lei, “Coordinated multipoint transmission with limited backhaul data transfer,” IEEE Trans. Wireless Commun., vol. 12, no. 6, pp. 2762–2775, Jun. 2013.

[17] Y. Cheng, M. Pesavento, and A. Philip, “Joint network optimization and downlink beamforming for CoMP transmissions using mixed integer conic programming,” IEEE Trans. Signal Process., vol. 61, no. 16, pp. 3972–3987, Aug. 2013.

[18] B. Dai and W. Yu, “Sparse beamforming and user-centric clustering for downlink cloud radio access network,” in IEEE Access, vol. 2, pp. 1326–1339, Oct. 2014.

[19] D. Donoho, “Compressed sensing,” IEEE Trans. Inf. Theory, vol. 52, no. 4, pp. 1289–1306, Apr. 2006.

[20] E. Candés and T. Tao, “Near-optimal signal recovery from random projections: Universal encoding strategies?” IEEE Trans. Inf. Theory, vol. 52, no. 12, pp. 5406–5425, Dec. 2006.

[21] F. Bach, R. Jenatton, J. Mairal, and G. Obozinski, “Optimization with sparsity-inducing penalties,” Foundations Trends Mach. Learning, vol. 4, no. 1, pp. 1–106, Jan. 2012.

[22] M. Sawahashi, Y. Kishiyama, A. Morimoto, D. Nishikawa, and M. Tanno, “Coordinated multipoint transmission/reception techniques for LTE-advanced [Coordinated and distributed MIMO],” IEEE Wireless Commun., vol. 17, no. 3, pp. 26–34, Jun. 2010.

[23] L. Choi and R.D. Murch, “A transmit preprocessing technique for multiuser MIMO systems using a decomposition approach,” IEEE Trans. Wireless Commun., vol. 2, no. 4, pp. 773–786, July 2003.

[24] S. W. Peters and R. W. Heath, Jr., “Cooperative algorithms for MIMO interference channels,” IEEE Trans. Veh. Technol., vol. 60, no. 1, pp. 206–218, Jan. 2011.

[25] C. Cartis, N. I. M. Gould, and P. H. L. Toint, “On the complexity of steepest descent, Newton’s and regularized Newton’s methods for nonconvex unconstrained optimization problems,” SIAM J. Optim., vol. 20, no. 6, pp. 2833–2852, Oct. 2010.

[26] M. Bengtsson and B. Ottersten, “Optimal and suboptimal transmit beamforming,” in Handbook of Antennas in Wireless Communications, L. C. Godara, Ed. Boca Raton, FL: CRC, Aug. 2001, ch. 18, pp. 1–18–33.

[27] Y. Huang and D. P. Palomar, “Rank-constrained separable semidefinite programming with applications to optimal beamforming,” IEEE Trans. Signal Processing, vol. 58, no. 2, pp. 664–678, Feb. 2010.

[28] S. Park, C.-B. Chae, and S. Bahk, “Before/after preceded massive MIMO in cloud radio access networks,” Proc. IEEE Int. Conf. on Comm., Jun. 2013.

[29] J. Kang, O. Simeone, J. Kang, and S. Shamai, “Downlink compression and precoding design for C-RANs over erodic fading channel,” Submitted to IEEE Trans. Veh. Technol., Online Available: http://arxiv.org/abs/1412.7713.

[30] S. W. Peters and R. W. Heath, Jr., “Cooperative algorithms for MIMO interference channels,” IEEE Trans. Veh. Technol., vol. 60, no. 1, pp. 206–218, Jan. 2011.
Long Bao Le (S’04-M’07-SM’12) received the B.Eng. degree in electrical engineering from Ho Chi Minh City University of Technology, Vietnam, in 1999, the M.Eng. degree in telecommunications from Asian Institute of Technology, Thailand, in 2002, and the Ph.D. degree in electrical engineering from the University of Manitoba, Canada, in 2007. He was a Postdoctoral Researcher at Massachusetts Institute of Technology (2008–2010) and University of Waterloo (2007–2008). Since 2010, he has been with the Institut National de la Recherche Scientifique (INRS), Université du Québec, Montréal, QC, Canada, where he is currently an associate professor. His current research interests include smart grids, cognitive radio, radio resource management, network control and optimization, and emerging enabling technologies for 5G wireless systems. He is a co-author of the book Radio Resource Management in Multi-Tier Cellular Wireless Networks (Wiley, 2013). Dr. Le is a member of the editorial board of IEEE TRANSACTIONS ON WIRELESS COMMUNICATIONS, IEEE COMMUNICATIONS SURVEYS AND TUTORIALS, and IEEE WIRELESS COMMUNICATIONS LETTERS. He has served as technical program committee chairs/co-chairs for several IEEE conferences including IEEE WCNC, IEEE VTC, and IEEE PIMRC.

Ngoc-Dung Dao (S’02-M’07) is a senior research engineer of Huawei Technologies Canada Co. Ltd. He received the Ph.D. degree from the University of Alberta, Canada in 2006. He has been with Siemens Communications Networks in Vietnam from 1995 to 2000, Toshiba Research Europe in the UK from 2007 to 2010. His recent research interests include SDN and NFV for radio access networks, information-centric networking (ICN), heterogeneous and dense networks, and reliable video communications for 5G mobile networks. Dr. Ngoc-Dung Dao is an editor of IEEE Transactions on Vehicular Technology, IEEE Communications Surveys and Tutorials, associate technical editor of IEEE Communications Magazine, and guest editor of 5G Special Issue of Eurasip Journal on Wireless Communications and Networking.