Charm physics confronts high-$p_T$ lepton tails

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ABSTRACT: We present a systematic survey of possible short-distance new-physics effects in (semi)leptonic charged- and neutral-current charmed meson decays. Using the Standard Model Effective Field Theory (SMEFT) to analyze the most relevant experimental data at low and high energies, we demonstrate a striking complementarity between charm decays and high invariant mass lepton tails at the LHC. Interestingly enough, high-$p_T$ Drell-Yan data offer competitive constraints on most new physics scenarios. Furthermore, the full set of correlated constraints from $K$, $\pi$ and $\tau$ decays imposed by SU(2)$_L$ gauge invariance is considered. The bounds from $D_{(s)}$ decays, high-$p_T$ lepton tails and SU(2)$_L$ relations chart the space of the SMEFT affecting semi(leptonic) charm flavor transitions.

KEYWORDS: Beyond Standard Model, Heavy Quark Physics

ArXiv ePrint: 2003.12421
1 Introduction

Understanding flavor transitions in the up-quark sector may prove crucial for unraveling the flavor puzzle and unveiling physics beyond the Standard Model (SM). A promising line in this direction is the investigation of transitions involving charmed hadrons. The recent discovery of direct CP violation in $D$ mesons decays [1] illustrates the maturity of this field and its potential to lead to new discoveries in the near future. In fact, an unprecedented amount of data on charm decays is expected to be collected at BES III [2], LHCb [3] and Belle II [4] experiments. Could this experimental program provide a charming gateway to new physics?
Leptonic and semileptonic charmed meson decays are an important benchmark in this program. These are exploited to determine the CKM matrix elements \([5, 6]\) and have been shown to be sensitive probes of New Physics (NP) \([7–9]\). On the other hand, the interpretation of hadron weak decays requires calculations of hadronic matrix elements in lattice QCD which in the charm sector are becoming available with increasing precision \([6, 10–16]\). Neutral-current decays are a priori more sensitive to NP because of the strong GIM suppression of the short-distance contributions in the up-quark sector \([17–23]\). Nonetheless, these are typically dominated by long-distance hadronic effects, which are difficult to treat from first principles \([23–27]\), hampering a direct theoretical interpretation of the data in terms of short-distance physics. In principle, both charged- and neutral-current decays could be affected by NP and the recent example of the \(B\)-meson anomalies \([28–38]\) prompts us to be open about the possible forms in which they could appear.

These anomalies have also fostered a more direct interplay between the traditional program of flavor physics at low energies and searches of NP in high-\(p_T\) tails at the LHC. Crossing symmetry allows one to connect univocally the decay and scattering amplitudes. If the NP scale is quite higher than the energies reached in the respective physical processes, this connection can be established model-independently using effective operators for the NP interactions. In high-energy proton-proton collisions, heavy flavors are virtually present in the initial states and can be produced in the final states. As required by unitarity arguments, above the electroweak (EW) scale the SM scattering amplitudes drop with energy while effective NP contributions keep growing. This energy-growing effect can compensate for the lower statistics in the high-\(p_T\) tails, and provide competitive probes to the traditional low-energy high-intensity program. This will become especially relevant with the upcoming high-luminosity phase at the LHC (HL-LHC) \([3]\).

The importance of combining low-energy data and high-\(p_T\) LHC data to constrain flavor-changing interactions has been already pointed out for the three light quarks \([39–41]\), the bottom quark \([42–46]\) and lepton-flavor violating interactions \([47–50]\), while there has not been a study devoted to the reach of this program in the charm sector.

In this work, we fill this gap by providing a comprehensive study of the interplay between the analyses of charmed-meson (semi)leptonic decays and high-\(p_T\) lepton tails at the LHC. In particular, we systematically explore the sensitivity of these experiments to possible short-distance NP in the charm sector using the Standard Model effective field theory (SMEFT) \([51, 52]\). The SMEFT provides a theoretical framework to describe NP effects originating above the EW scale, which is well-motivated given the lack of direct observation of new resonances at the LHC, and the consistency of the observed properties of the Higgs boson with the SM. Using the SMEFT, we can establish a link between charm decays and the production of high-\(p_T\) leptons at the LHC. Moreover, due to its manifest SU(2)\(_L\) gauge invariance, this framework allows to establish correlations with kaon and tau physics.

The next four sections investigate, in steps, charged-current transitions. Namely, starting from the effective field theory setup in section 2, we study the set of constraints from charmed meson decays in section 3, the production of monoleptons at high-\(p_T\) LHC in section 4 and, finally, compare the two in section 5. The analysis is then repeated for neutral-current transitions in section 6. Complementary constraints implied by SU(2)\(_L\) gauge symmetry are derived in section 7. We conclude in section 8.
2 Theoretical framework: $c \to d^* \bar{e} \alpha \nu^\beta$

2.1 The high-energy effective theory

We focus on short-distance NP that can affect semileptonic charged-current charm transitions, particularly when charm number changes by one unit, $\Delta C = 1$. Under the assumption of no new degrees of freedom below (or at) the electroweak scale, NP effects can be fully described employing the SMEFT. The relevant Lagrangian is

$$\mathcal{L}_{\text{SMEFT}} \supset \frac{1}{v^2} \sum_k C_k \mathcal{O}_k,$$

(2.1)

where $v \approx 246$ GeV is the SM Higgs vacuum expectation value and the Wilson coefficients (WCs) scale as $C_k \propto v^2/\Lambda^2$, with $\Lambda$ being the scale of NP. We employ the Warsaw basis [52] for operators of canonical dimension six, which is particularly suited for flavor physics as covariant derivatives and field strengths are reduced in favor of fermionic currents using the equations of motion. The most general set of semileptonic four-fermion SMEFT operators contributing to $c \to d^* \bar{e} \alpha \nu^\beta$ transitions are

$$\mathcal{O}^{(3)}_{\ell q} = (\bar{l}_L \gamma_\mu \tau^I l_L)(\bar{q}_L \gamma^\mu \tau^I q_L), \quad \mathcal{O}_{\ell dq} = (\bar{l}_L e_R)(\bar{d}_R q_L),$$

(2.2)

$$\mathcal{O}^{(1)}_{\text{lequ}} = (\bar{p}_L \bar{e}_R) \epsilon_{pr} (\bar{q}_L u_R), \quad \mathcal{O}^{(3)}_{\text{lequ}} = (\bar{p}_L \sigma_{\mu \nu} e_R) \epsilon_{pr} (\bar{q}_L \sigma^{\mu \nu} u_R),$$

with $\sigma^{\mu \nu} = \frac{i}{2} [\gamma^\mu, \gamma^\nu]$, $\tau^I$ the Pauli matrices, $\epsilon_{pr}$ the Levi-Civita symbol and $\{p, r\}$ being SU(2)$_L$ indices. The left-handed quark and lepton doublets are denoted by $q_L$ and $l_L$, respectively, while the right-handed singlets are $u_R$, $d_R$ and $e_R$. On the other hand, the SMEFT operators that modify the $W$ couplings to quarks read

$$\mathcal{O}^{(3)}_{\phi q} = (\phi^\dagger i D_\mu \phi)(\bar{q}_L \gamma^\mu \tau^I q_L), \quad \mathcal{O}_{\phi ud} = (\phi^\dagger i D_\mu \phi)(\bar{u}_R \gamma^\mu d_R),$$

(2.3)

where $\phi$ is the Higgs field and $D_\mu$ its covariant derivative. We neglect the chirality-flipping $W$ vertices of the type $\bar{\psi} \sigma^{\mu \nu} \psi F^\mu_{\nu}$. Their effects are subleading relative to the operators in eq. (2.3) at low-energies, since they are charm mass suppressed, and to the operators in eq. (2.2) at high-$p_T$, due to their different high-energy behavior discussed in section 4.1. We also neglect all modifications to the leptonic $W$ vertices, since they are better probed in purely leptonic transitions.

Thus, the operators in eqs. (2.2) and (2.3) capture all leading effects in the SMEFT in semileptonic charm transitions. Unless stated otherwise, throughout this paper we work in the up-basis for the SU(2)$_L$ multiplets, where

$$q^i_L = \begin{pmatrix} u^i_L \\ V_{ij} d^j_L \end{pmatrix}, \quad l^i_L = \begin{pmatrix} v^i_L \\ e^i_L \end{pmatrix},$$

(2.4)

with $V$ the CKM matrix, and use $i, j = 1, 2, 3$ and $\alpha, \beta = 1, 2, 3$ to label quark and lepton flavor indices, respectively. We also use $\ell$ to denote the light leptons $e$ and $\mu$, but not $\tau$. The matching of the SMEFT to the low-energy effective theory is reported next, while we postpone the discussion of SU(2)$_L$ relations to section 7.

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2.2 The low-energy effective theory

The low-energy effective Lagrangian involving $e \to d \bar{e} \bar{\nu} \nu$ transitions can be written as

$$\mathcal{L}_{CC} = -\frac{4 G_F}{\sqrt{2}} V_{ei} \left[ (1 + \epsilon^{\alpha \beta i}_{V_L}) \mathcal{O}^{\alpha \beta i}_{V_L} + \epsilon^{\alpha \beta i}_{V_R} \mathcal{O}^{\alpha \beta i}_{V_R} + \epsilon^{\alpha \beta i}_{S_L} \mathcal{O}^{\alpha \beta i}_{S_L} + \epsilon^{\alpha \beta i}_{S_R} \mathcal{O}^{\alpha \beta i}_{S_R} + \epsilon^{\alpha \beta i}_{T} \mathcal{O}^{\alpha \beta i}_{T} \right] + \text{h.c.},$$

(2.5)

where the effective operators read

$$\mathcal{O}^{\alpha \beta i}_{V_L} = (\bar{e}_L^\alpha \gamma_{\mu} \nu_L^\beta)(\bar{c}_L \gamma_{\mu} d_L^i), \quad \mathcal{O}^{\alpha \beta i}_{V_R} = (\bar{e}_L^\alpha \gamma_{\mu} \nu_R^\beta)(\bar{c}_R \gamma_{\mu} d_R^i),$$

$$\mathcal{O}^{\alpha \beta i}_{S_L} = (\bar{e}_R^\alpha \nu_L^i)(\bar{e}_R d_L^i), \quad \mathcal{O}^{\alpha \beta i}_{S_R} = (\bar{e}_R^\alpha \nu_R^i)(\bar{c}_L d_R^i),$$

$$\mathcal{O}^{\alpha \beta i}_{T} = (\bar{e}_R^\alpha \sigma_{\mu \nu} \nu_R^i)(\bar{c}_R \sigma_{\mu \nu} d_R^i).$$

(2.6)

Note that mixed chirality tensor operators vanish by Lorentz invariance. The extraction of the CKM matrix in the SMEFT is a delicate exercise [54]. For our purposes here, $V_{cd}$ and $V_{cs}$ can be safely obtained by exploiting unitarity in the Wolfenstein parametrization,

$$V_{cd} = -\lambda_c + \mathcal{O}(\lambda_c^2),$$
$$V_{cs} = 1 - \frac{\lambda_c^2}{2} + \mathcal{O}(\lambda_c^4),$$

(2.7)

where $\lambda_c$ is the sine of the Cabibbo angle. We assume that any contribution of NP to the inputs of these unitarity relations is small compared to the precision achieved with charm weak transitions. For instance, $\lambda_c$ obtained from kaon decays receives strong constraints from the unitarity of the first row of the CKM matrix (see e.g. ref. [40]). Similarly, we neglect the effects of NP modifications to $G_F$ as determined from muon decays.

The tree-level matching conditions between the SMEFT in eq. (2.1) and the low-energy Lagrangian in eq. (2.5) are

$$\epsilon^{\alpha \beta i}_{V_L} = -\frac{V_{ji}}{V_{ei}} \left[ C^{(1)}_{ij} \right]_{\alpha \beta 2j} + \delta_{\alpha \beta} \frac{V_{ji}}{V_{ei}} \left[ C^{(1)}_{ij} \right]_{\alpha \beta 2j}, \quad \epsilon^{\alpha \beta i}_{V_R} = \frac{1}{2 V_{ei}} \delta_{\alpha \beta} \left[ C_{\nu \delta q} \right]_{2i},$$

$$\epsilon^{\alpha \beta i}_{S_L} = -\frac{V_{ji}}{2 V_{ei}} \left[ C^{(1)}_{ij} \right]_{\beta \alpha j 2}, \quad \epsilon^{\alpha \beta i}_{S_R} = -\frac{1}{2 V_{ei}} \left[ C_{\nu \delta q} \right]_{2i} \left[ C_{\nu \delta q} \right]_{2i} \delta_{\alpha \beta},$$

$$\epsilon^{\alpha \beta i}_{T} = -\frac{V_{ji}}{2 V_{ei}} \left[ C^{(1)}_{ij} \right]_{\beta \alpha j 2} \delta_{\alpha \beta}.$$ 

(2.8)

where a sum over $j$ is implicitly assumed. Interestingly, the low-energy operator $\mathcal{O}^{\alpha \beta i}_{V_R}$ is generated in the SMEFT from an operator that modifies a chirality preserving $W$ vertex but not from a new four-fermion interaction, unlike other operators in eq. (2.6). On the contrary, $\mathcal{O}^{\alpha \beta i}_{V_L}$ receives contributions from both a modified $W$ vertex and a new four-fermion interaction, which cannot be disentangled at low energies.

The relations in eq. (2.8) hold at the matching scale $\mu = m_W$. The renormalization group equations (RGE) induced by QCD and EW (QED) radiative effects allow one to robustly correlate low- and high-$p_T$ data [55, 56]. In particular, the RGE running from $\mu = 1 \text{ TeV}$ down to $\mu = 2 \text{ GeV}$ yields sizable effects in scalar and tensor operators [57],

$$\epsilon_{S_L}(2 \text{ GeV}) \approx 2.1 \epsilon_{S_L}(\text{TeV}) - 0.3 \epsilon_T(\text{TeV}), \quad \epsilon_{S_R}(2 \text{ GeV}) \approx 2.0 \epsilon_{S_R}(\text{TeV}),$$

$$\epsilon_T(2 \text{ GeV}) \approx 0.8 \epsilon_T(\text{TeV}).$$

(2.9)
Here, $\epsilon_X$ (TeV) refers to the corresponding combination of SMEFT WCs in eq. (2.8). Vector operators do not run under QCD, and the electromagnetic and EW running remains at the percent level. Similarly, other RGE-induced contributions, including the mixing with other SMEFT operators, do not receive large QCD enhancements and remain at the percent level. All these effects are below the level of precision of our studies, so we neglect them in the following.

3 Decays of charmed mesons

Leptonic and semileptonic decays $D_{(s)} \rightarrow \bar{e}^{\alpha} \nu$ and $D \rightarrow \pi (K) \ell \nu$ follow from the Lagrangian in eq. (2.5). This captures the leading effects of any possible short-distance contribution to $c \rightarrow d \bar{e}^{\alpha} \nu^\beta$ flavor transitions, with the SM being a particular limit, $\epsilon^{\alpha \beta \beta}_{X,SM} = 0$ for all $X$. Hadronic matrix elements of the corresponding operators are constrained by Lorentz symmetry and invariance of QCD under parity. As a result, pure leptonic decays are sensitive only to axial ($\epsilon^{\alpha \beta \beta}_A = \epsilon^{\alpha}_{V_R} - \epsilon^{\alpha}_{V_L}$) and pseudoscalar ($\epsilon^{\alpha \beta \beta}_P = \epsilon^{\alpha \beta}_{S_R} - \epsilon^{\alpha \beta}_{S_L}$) combinations of WCs. On the other hand, the semileptonic decays are sensitive to vectorial ($\epsilon^{\alpha \beta \beta}_V = \epsilon^{\alpha \beta}_{V_R} + \epsilon^{\alpha \beta}_{V_L}$) and scalar ($\epsilon^{\alpha \beta \beta}_S = \epsilon^{\alpha \beta}_{S_R} + \epsilon^{\alpha \beta}_{S_L}$) combinations of WCs, and to the tensor WC ($\epsilon^{\alpha \beta \beta}_T$).

The largest available phase space that can be achieved for the semileptonic decays is given by $m_{D^+} - m_{e^\nu} \approx 1.735$ GeV. Note that this is smaller than the $	au$ lepton mass, which makes the semitauonic $D$-meson decays kinematically forbidden. A similar conclusion follows for the decays of charmed baryons. In other words, the tauonic vector, scalar and tensor operators ($O^{V,S,T}_{\nu \ell \nu}$) are not directly accessible and, as we will see below, high-$p_T$ tails provide a unique probe of these operators. On the other hand, pure tauonic decays of $D_{(s)}$ are allowed.\footnote{The phase-space restriction is lifted for semitauonic decays of excited $D^*$ mesons. However, these predominantly decay electromagnetically or strongly and the branching fractions of weak decays are suppressed \cite{58, 59}. Furthermore, one could in principle access the tauonic tensor operator by measuring $D_{(s)} \rightarrow \tau \nu \gamma$ (see e.g. ref. \cite{40} for the equivalent pion and kaon decays).}

In the following, we derive bounds on the WCs of the operators in eq. (2.6) from $D_{(s)}$-meson decays. First, we restrict ourselves to the lepton-flavor diagonal case ($\epsilon^{\nu \alpha}_{\ell \nu} \equiv \epsilon^{\nu \alpha}_{\ell \nu}$), which interferes with the SM and leads to the strongest bounds. The rate of the leptonic $D$ decays is

$$BR(D^+ \rightarrow \bar{e}^{\alpha} \nu^\alpha) = \tau_{D^+} \frac{m_{D^+} m_D^2 f_D^2 G_F^2 |V_{cd}|^2 \beta^2_a}{8\pi} \left| 1 - \epsilon^a_A + \frac{m_D^2}{m_\alpha (m_c + m_u)} \epsilon^a_{P} \right|^2,$$

where $\beta^2_a = 1 - m_\alpha^2/m_D^2$ and $\tau_{D^+}$ ($f_{D^+}$) is the $D^+$ lifetime (decay constant). This formula with obvious replacements also describes the leptonic $D_s$ decays. We use $f_D = 212.0(7)$ MeV and $f_{D_s} = 249.9(5)$ MeV, obtained from an average of lattice QCD simulations with two degenerate light quarks and dynamical strange and charm quarks in pure QCD \cite{6, 10, 11}. An important feature of the leptonic decays is that the axial contribution, such as the one predicted in the SM, is suppressed by $m_\alpha^2$ due to the conservation of angular momentum. On the contrary, pseudoscalar NP contributions are unsuppressed, and they receive strong constraints from searches and measurements of these decays.
In the case of semileptonic $D$ decays, the expressions for total rates are more involved as they contain kinematic integrals with form factors, which are functions of the invariant mass of the dilepton pair. The decay rate of the neutral $D$ meson can be parametrized as a function of the WCs,

$$\text{BR}(D \to P_i \ell^+ \nu) = \frac{\prod_{\alpha} \text{BR}_{\text{SM}} \prod_{\alpha} x_{S,T} \prod_{\alpha} y_{S,T}}{\prod_{\alpha} |\epsilon_{\ell^+}^{\alpha}|^2 + 2 \text{Re} [(1 + \epsilon_{\ell^+}^{\alpha})(x_S \epsilon_{S}^{\alpha*} + x_T \epsilon_{T}^{\alpha*})] + y_S |\epsilon_{S}^{\alpha*}|^2 + y_T |\epsilon_{T}^{\alpha*}|^2},$$

(3.2)

where $x_{S,T}$ and $y_{S,T}$ describe the interference between NP and SM and the quadratic NP effects, respectively, and $P_i = \pi, K$ for $i = d, s$. The numerical values of these parameters can be obtained using lattice QCD calculations of the form factors and performing the kinematic integrals. In table 1 we show the values of these parameters for the $D^0 \to \pi^-(K^-)\ell^+\nu$ decays using the lattice results from [15, 16]. The errors in the parametrization employed in these references have been propagated consistently.

The limits on the WCs are determined by comparing these predictions to the PDG averages [60] of the experimental data on the branching fractions [61–74]. The results are shown in table 2 where one WC is fitted at a time setting the rest to zero. The sensitivity to vectorial currents is at the few percent level, reflecting the precision achieved in the experimental measurements and in the calculation of the respective semileptonic form factors. Bounds on axial currents depend strongly on the lepton flavor due to the chiral suppression of their contributions to the leptonic-decay rates. Thus, the electronic axial operators are poorly constrained while muonic ones are constrained down to a few percent. The difference between $cs$ and $cd$ transitions in the bounds on the tauonic axial contributions is a result of the different experimental precision achieved in the measurement of the corresponding decays.

Direct bounds on scalar and tensor operators stemming from semileptonic decays are rather weak, with almost $O(1)$ contributions still allowed by the data. As shown in table 1, this is due to the fact that the interference of these operators with the SM is chirally suppressed (see e.g. ref. [40]) and the bound is on their quadratic contribution to the rates. Pseudoscalar contributions to the leptonic-decay rates are, on the other hand, chirally enhanced with respect to the SM contribution and, as a result, constrained down to the per-mille level for electronic and muonic channels. For the tauonic ones, the lepton-mass enhancement is absent, and the bounds are $\sim 1\%$ ($cs$) or $\sim 10\%$ ($cd$), depending again on the experimental uncertainties.

| $P$ | $\alpha$ | $\text{BR}_{\text{SM}}$ | $x_S$ | $x_T$ | $y_S$ | $y_T$ |
|-----|-----|--------------------|-----|-----|-----|-----|
| $\pi^-$ | $e$ | $2.65(18) \cdot 10^{-3}$ | $1.12(10) \cdot 10^{-3}$ | $1.21(15) \cdot 10^{-3}$ | $2.74(22)$ | $1.14(21)$ |
|     | $\mu$ | $2.61(17) \cdot 10^{-3}$ | $0.228(19)$ | $0.23(3)$ | $2.73(18)$ | $1.15(22)$ |
| $K^-$ | $e$ | $3.48(26) \cdot 10^{-2}$ | $1.29(8) \cdot 10^{-3}$ | $1.18(11) \cdot 10^{-3}$ | $2.00(11)$ | $0.69(8)$ |
|     | $\mu$ | $3.39(25) \cdot 10^{-2}$ | $0.251(16)$ | $0.224(20)$ | $2.00(11)$ | $0.71(8)$ |

Table 1. Coefficients of the parametrization in eq. (3.2) obtained using lattice QCD results [15, 16] for the form factors.
the bounds reported in tables 2 and 3 from the modes analyzed in this work will remain
radiative (QED) effects (see LQCD projections in ref. [3]). In summary, improvements of
required in the computation of the corresponding hadronic matrix elements, including
in the SM prediction of these decay modes will be challenging because of the precision
likely be limited by systematic uncertainties. Moreover, going beyond
\sim 10^5\text{ab}^{-1}
decays, the data samples are expected to increase by two orders of magnitude after the
in ref. [2]), while no projections for electronic decays have been provided. For semileptonic
decays, assuming them to be real.

From the model building perspective, at a scale $\Lambda > v$, the NP effects are naturally
realized in terms of operators in the chiral basis. Models for which the dominant contribution
is through scalar operators receive the strongest constraint from leptonic decays, unless
some tuning between $O_{S_L}$ and $O_{S_R}$ is enforced. In addition, scalar and tensor operators
receive radiative contributions that rescale and mix them significantly when connecting
the direct bounds in table 2 to the matching scale, cf. eq. (2.9). Or, inversely, a model
producing a tensor contribution at the matching scale will produce a scalar contribution
at low energies that is then constrained by leptonic decays. This is illustrated in table 3
where we have expressed the low-energy bounds in terms of the WCs in the chiral basis at
$\mu = 1\text{TeV}$. As expected, bounds on single scalar and tensor operators are dominated by
the measurements of pure leptonic decays.

Except for operators whose dominant contribution to the observables is already
quadratic ($O_{S,L}^{\alpha\beta}$ and $O_{S,R}^{\alpha\beta}$), the limits in table 2 are weakened if NP does not interfere
with the SM. This is the case when the neutrino flavor is $\beta \neq \alpha$, or when the WCs are
imaginary. The bounds are relaxed typically by a factor $\sim 3-6$ over the symmetrized
ranges shown in that table. However, for a few operators, namely $O_{A,P}^{\alpha\beta}$, $O_{A,P}^{\tau\rho}$ and $O_{V}^{\beta\nu}$,
the worsening is by an order of magnitude. Therefore, in the absence of SM interference,
the bounds from $D_{(s)}$ meson decays are weak except for the pseudoscalar operators, which
can still be competitive with other constraints.

Improvements on purely muonic and tauonic branching fractions by a factor $\sim 2-3$ are
expected from future measurements at BES III [2] and Belle II [4] (see detailed projections
in ref. [2]), while no projections for electronic decays have been provided. For semileptonic
decays, the data samples are expected to increase by two orders of magnitude after the
full 50 $\text{ab}^{-1}$ of integrated luminosity planned at Belle II [4], thus the precision will most
likely be limited by systematic uncertainties. Moreover, going beyond $\sim 1\%$ accuracy
in the SM prediction of these decay modes will be challenging because of the precision
required in the computation of the corresponding hadronic matrix elements, including
radiative (QED) effects (see LQCD projections in ref. [3]). In summary, improvements of
the bounds reported in tables 2 and 3 from the modes analyzed in this work will remain
modest in the near future.

| $i$ | $\alpha$ | $\epsilon_{V}^{\alpha i}$ | $\epsilon_{A}^{\alpha i}$ | $\epsilon_{S}^{\alpha i}$ | $\epsilon_{P}^{\alpha i}$ | $\epsilon_{T}^{\alpha i}$ |
|-----|----------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| d   | e        | $[-0.02, 0.11]$          | $[-32, 34]$               | $[-0.29, 0.29]$          | $[-0.005, 0.005]$        | $[-0.5, 0.5]$            |
|     | $\mu$    | $[-0.06, 0.07]$          | $[-0.013, 0.07]$          | $[-0.33, 0.17]$          | $[-0.0024, 0.0004]$      | $[-0.6, 0.22]$           |
|     | $\tau$   | 0                        | $[-0.27, 0.21]$          | 0                        | $[-0.11, 0.15]$         | 0                        |
| s   | e        | $[-0.07, 0.08]$          | $[-27, 29]$               | $[-0.29, 0.29]$          | $[-0.005, 0.004]$        | $[-0.5, 0.5]$            |
|     | $\mu$    | $[-0.09, 0.06]$          | $[-0.07, 0.02]$          | $[-0.4, 0.16]$          | $[-0.0007, 0.0022]$      | $[-0.9, 0.22]$           |
|     | $\tau$   | 0                        | $[-0.07, 0.014]$         | 0                        | $[-0.008, 0.04]$        | 0                        |

Table 2. 95% CL ranges of the WCs of the charged-current operators obtained at the scale
$\mu = 2\text{GeV}$ from current experimental data on (semi)leptonic $D_{(s)}$-meson decays, assuming them to be real.
Table 3. 95% CL ranges of the WCs, assumed to be real, obtained from $D_{(s)}$-meson decays for scalar and tensor operators in the chiral basis at $\mu = 1$ TeV. The ranges of $\epsilon_{SR}^S$ are those of $-\epsilon_{SL}^S$.

| $\alpha$ | $\epsilon_{SL}^S (\epsilon_{SR}^S) \times 10^3$ | $\epsilon_T^S \times 10^2$ |
|---------|-----------------------------|-----------------------------|
| $e$     | $[-2.5, 2.7]$               | $[-1.6, 1.5]$               |
| $\mu$   | $[-0.2, 1.2]$               | $[-0.7, 0.13]$              |
| $\tau$  | $[-70, 60]$                 | $[-33, 44]$                 |
| $e$     | $[-2.0, 2.2]$               | $[-1.3, 1.2]$               |
| $\mu$   | $[-1.1, 0.3]$               | $[-0.2, 0.6]$               |
| $\tau$  | $[-19, 4.0]$                | $[-2.0, 12]$                |

Finally, it is important to stress that we have restricted our analysis to decay channels for which precise measurements and accurate LQCD predictions of the form factors currently exist. Additional modes that can be considered are $D \to V \ell \nu$ decays ($V = \rho, K^*$), for which modern lattice results do not exist [9], or baryonic $\Lambda_c$ decays for which data is not very precise yet. In addition, one may consider other observables such as kinematic distributions. Including these observables may improve the bounds on some of the WCs in the future and close flat directions in a global fit of decay data (see e.g. ref. [9]).

4 High-$p_T$ lepton production at the LHC

4.1 Short-distance new physics in high-$p_T$ tails

The monolepton production in proton-proton collisions at high-energy, $\sqrt{s} \gg m_W$, is an excellent probe of new contact interactions between quarks and leptons.\(^3\) The final state in this process features missing energy plus a charged lepton of three possible flavors. In addition, there are five quark flavors accessible in the incoming protons whose composition is described by the corresponding parton distribution functions (PDF). Within the SMEFT, a total of 4 four-fermion operators contribute to this process at tree-level for each combination of quark and lepton flavors, see eq. (2.2). Their contribution to the partonic cross section grows with energy as $\hat{\sigma} \propto s$, see eq. (4.2). Other effects in the SMEFT include the chirality preserving (flipping) $W$-boson vertex corrections which scale as $\hat{\sigma} \propto s^{-1} (s^0)$ and are negligible in the high-$p_T$ tails compared to the four-fermion interactions.\(^4\)

The numerical results derived in this work are based on the Monte Carlo simulations described in section 4.2. Here we present a (semi-)analytic understanding of the main physical effects. The tree-level unpolarized partonic differential cross section for $d^j(p_1) \bar{u}^i(p_2) \to e^\alpha(p_3) \bar{\nu}^\beta(p_4)$, induced by the SMEFT four-fermion operators in eq. (2.2),

\(^3\)There is a rich literature of NP exploration in neutral and charged Drell-Yan production, for an incomplete list see [39–43, 45, 46, 48, 75–81].

\(^4\)The modification of the $W$-boson propagator in the universal basis [82] through the $\hat{W}$ parameter is captured by the specific combination of the four-fermion contact interactions and vertex corrections in the Warsaw basis. For $\hat{W}$ searches in the high-$p_T$ lepton tails see ref. [76].
expanded and matched to the notation of eq. (2.5), is
\[
d\hat{\sigma}/dt = \frac{G_F^2 |V_{ij}|^2}{2 \pi s^2} \left[ (s + t) \left| \delta_{\alpha\beta} \frac{m_W^2}{s} - \epsilon_{V_L}^{\alpha\beta ij} \right|^2 + \frac{s^2}{4} \left( |\epsilon_{S_L}^{\alpha\beta ij}|^2 + |\epsilon_{S_R}^{\alpha\beta ij}|^2 \right) + 4(s + 2t) |\epsilon_T^{\alpha\beta ij}|^2 \right]
\]
\[ - 2s(s + 2t) \text{Re}\left( \epsilon_{S_L}^{\alpha\beta ij} \epsilon_T^{\alpha\beta ij} \right) \],

(4.1)

where \( s \equiv (p_1 + p_2)^2 \) and \( t = (p_3 - p_1)^2 \) are the corresponding Mandelstam variables. The interference with the SM is relevant for \(|\epsilon_{V_L}| \sim m_W^2/\text{TeV}^2 \) or smaller. This holds irrespective of the initial quark flavors in \( d^i \bar{u}^j \rightarrow e^a \bar{\nu}^a \) (\( i = 1, 2 \) and \( j = 1, 2, 3 \)). The results obtained in our numerical analysis (see table 4) suggest that the quadratic term in \( \epsilon_{V_L} \) dominates present limits. However, there is already a non-negligible correction from the interference term which will become prominent with more integrated luminosity. The lack of interference in the other cases tends to increase the cross section in the high-\( p_T \) tails, and allows to extract bounds on several NP operators simultaneously.\(^5\) On the contrary, most of the bounds from \( D_{(s)} \) mesons decays discussed in section 3 depend on interference terms among different WCs, and it becomes difficult to break flat directions without additional observables.

While the energy growth of the amplitude enhances the signal, the PDF of the sea quarks reduce it. The parton luminosity for colliding flavors \( i \) and \( j \) is
\[
\mathcal{L}_{q_i \bar{q}_j}(\tau, \mu_F) = \int_1^1 dx \frac{d \sigma}{dx} f_{q_i}(x, \mu_F) f_{\bar{q}_j}(\tau/x, \mu_F),
\]
(4.3)

where \( \tau = s/s_0 \) and \( \sqrt{s_0} \) is the collider energy (here set to 13 TeV). The relative correction to the Drell-Yan cross section in the tails (\( \sqrt{s} \gg m_W \)) is
\[
\frac{\Delta \sigma}{\sigma} \approx R_{ij} \frac{d \sigma}{(m_W^2/s)^2},
\]
(4.4)

with \( d_X = 1, \frac{3}{4}, 4 \) for \( X = V, S, T \) respectively, and
\[
R_{ij} \equiv \frac{(\mathcal{L}_{u_d j_1} + \mathcal{L}_{d_j u_1}) \times |V_{ij}|^2}{(\mathcal{L}_{u_d} + \mathcal{L}_{d u}) \times |V_{ad}|^2}.
\]
(4.5)

We show in figure 1 the ratios \( R_{ij} \) for \( d u \) (red dashed), \( d c \) (red solid), \( s u \) (blue dashed), \( s c \) (blue solid), \( b u \) (green dashed) and \( b c \) (green solid) as a function of the dilepton invariant mass \( \sqrt{s} \). Here we use the MMHT2014 NNLO188 PDF [83] with the factorization

\(^5\)The transverse mass distribution \( (m_T \approx 2 p_T) \) also inherits negligible \( \epsilon_{S_L} - \epsilon_T \) interference.
Figure 1. Suppression factors for the charged-current Drell-Yan cross section with different colliding quark flavors, $R_{ij}$, stemming from the PDF and the CKM matrix, see eq. (4.5).

The suppression from $R_{ij}$ is compensated by the energy enhancement $(\sqrt{s}/m_W)^{4} \sim O(10^5)$. Thus, a measurement of the cross section in the tails with $O(10\%)$ precision would probe $cs$ and $cd$ at the level of $\epsilon_X \sim O(10^{-2})$. The weak dependence on the energy across the most sensitive bins allows to rescale the limits for different flavor combinations provided the lepton cuts are sufficiently inclusive (see section 4.2).

The Drell-Yan production in the SM is known at NNLO QCD and NLO EW (see e.g. refs. [84, 85]). The theoretical prediction for our signal rate is plagued by the uncertainties stemming from the missing high-order perturbative corrections, as well as the knowledge of the PDF of the colliding sea quarks. These have been studied in detail in [42, 45]. More precisely, NLO QCD and PDF uncertainties are quantified in the supplemental material of ref. [45] for a $bc \to W'$ example (and in ref. [42] for $bb \to Z'$) as a function of the vector boson mass $m_{V'}$. These estimates are trivially applicable for the corresponding quark-lepton contact interactions when replacing $m_{V'}$ with the dilepton invariant mass $\sqrt{s}$. A relative uncertainty of $\sim 10\%$ is found on the differential cross section in the most sensitive bins. Electroweak corrections can also be at this level in this kinematical region. Another potential issue comes from the PDF extraction, as recent analyses also include Drell-Yan data, see e.g. ref. [86]. While at the moment this data has a subleading impact on the PDF determination, it will become important at the HL-LHC [87]. A proper approach would be to perform a combined SMEFT and PDF fit. First steps in this direction show discriminating power between EFT and PDF effects in the context of deep inelastic scattering [88].

4.2 Recast of the existing experimental searches

We use the analyses reported by ATLAS and CMS collaborations with one lepton plus missing transverse momentum signature. For the $\tau + \nu$ channel, we recast the searches in refs. [89, 90] using 36.1 fb$^{-1}$ and 35.9 fb$^{-1}$ of data, respectively. In the case of $\ell + \nu$ final state, we use the ATLAS 139 fb$^{-1}$ [91] and the CMS 35.9 fb$^{-1}$ [92] analyses. The Monte Carlo
(MC) simulation pipeline is as follows: we use FeynRules [93] for the model generation,
MadGraph5_aMC@NLO [94, 95] for the partonic process simulation interfaced with Pythia 8 [96] to simulate the hadronic processes, and finally Delphes [97] to get an estimate of
the detector effects. We set a dynamical scale for renormalization and factorization scales, \( \mu_{R/F} = m_T \). We use the ATLAS and CMS Delphes cards, respectively, when making the simulations for each experiment. ROOT [98] is used to apply the selection criteria of each
analysis to the corresponding Delphes output, and to obtain the expected yields for our
signals in each bin of the reported transverse mass distributions.

We validated our setup by producing MC samples for \( W \to e^+\nu + \text{jets} \) in the SM, and comparing the yields with those reported by ATLAS and CMS. We reproduce their results within 10% to 20% accuracy. As we only use limited MC simulation capabilities, detector emulation via Delphes, and no experimental corrections from data, as done in
the experimental analyses, we consider this level of agreement as an accurate reproduction
of the experimental results from the phenomenological perspective. The same techniques
have been used and reported in [45]. Thus, the relative error on the limits derived here
from the high-\( p_T \) data is expected to be below 10% \( \Delta \epsilon_X / \epsilon_X \approx 0.5 \Delta \sigma / \sigma \).

The limits on the WCs are obtained by comparing our simulated signal events for the
transverse mass distributions to the background events in the corresponding collaboration
analyses. For the statistical analysis, we use the modified frequentist CLs method [99].
We compute the CLs using the ROOT package Tlimit [100], and exclude WC values with
CLs < 0.05. In our statistical analysis, we include the SM background systematic and statistical errors (added in quadrature) provided by the collaborations for all bins. We ignore any possible correlation in the bin errors when combining the bins, since these
are not provided. For the vector operator, both NP-squared and NP-SM interference
contributions are computed. We do not include systematic errors for the signal simulation
in our analysis, as they are expected to be subdominant compared to the overall signal
normalization uncertainty stemming from the theoretical prediction of the cross section
discussed in section 4.1.

Our results are reported in table 4 in terms of the WCs at two different scales \( \mu = 1 \text{ TeV} \)
and \( \mu = 2 \text{ GeV} \), respectively.\(^6\) The resulting limits qualitatively agree with the naive ratios
in the absence of SM-NP interference,

\[
\epsilon^{\alpha \beta i}_{V_L} : \epsilon^{\alpha \beta i}_{S_{L,R}} : \epsilon^{\alpha \beta i}_{T} \approx 1 : \frac{2}{\sqrt{3}} : \frac{1}{2},
\]  

(4.6)
due to rather inclusive kinematics of the analysis. A dedicated future analysis should
exploit the angular dependence in eq. (4.1) in order to differentiate among operators, and
possibly further suppress the background. We also recommend separating future data by
the lepton charge as a way to further enhance the signal over background discrimination.
For instance, \( ud \)-induced monolepton production is asymmetric in lepton charge unlike \( cs \).
Further improvements in sensitivity could be obtained by tagging an additional (soft) jet.

\(^6\)See eq. (2.9) for the RGE solutions. The difference between \( S_L \) and \( S_R \) is \( \mathcal{O}(1\%) \) so we use a single column.
The corresponding partonic cross section including both SM and the EFT with the normalization chosen such that

\[ |\epsilon_{V_L}^{\alpha\beta}| \times 10^2 \quad (\alpha \neq \beta) \]

\[ |\epsilon_{S_{LR}}^{\alpha\beta}(\mu)| \times 10^2 \quad \mu = 1 \text{ TeV} \]

\[ |\epsilon_{T}^{\alpha\beta}(\mu)| \times 10^3 \quad \mu = 2 \text{ GeV} \]

Table 4. 95% CL limits on the value of the WC's of the charged-current operators obtained from high-\( p_T \) data (\( \beta = e, \mu, \tau \)). We also show in parenthesis the naive projections for the HL-LHC (3 ab\(^{-1}\)) on the expected limits, assuming that the error will be statistically dominated.

For the \( \tau + \nu \) channel, the reported limits are well compatible with those obtained by naive rescaling via the \( R_{ij} \) ratios in eq. (4.5) of the ones presented in ref. [45] (neglecting the interference for \( \epsilon_{V_L} \)). In principle, this method can be used to estimate the limit on any \( u^i \rightarrow d^j \) transition. Finally, the jackknife analysis performed in the supplemental material of [45] suggests that the most sensitive bins in these types of searches to fall in the range between 1 and 1.5 TeV. This raises questions about the applicability of the high-\( p_T \) bounds to the space of possible NP models modifying charged-current charm transitions, to which we turn next.

### 4.3 Possible caveats within and beyond the EFT

As shown in section 4.2, most of the limits obtained from high-\( p_T \) tails are stronger than their low-energy counterparts. However, one could argue that high-\( p_T \) limits are not free of caveats, which would allow certain NP models to evade them while still yielding sizeable low-energy contributions.

For concreteness, let us first remain within the realm of the SMEFT, where any new degree of freedom is well above the EW scale. The partonic cross-section for \( \bar{c}d^i \rightarrow e^{\alpha}\bar{\nu}^{\alpha} \) scattering in the presence of dimension-six operators is given in eq. (4.2). As can be seen from this expression, the NP-squared piece receives an energy enhancement with respect to both the pure SM contribution and SM-NP interference. As a result, the limits shown in table 4 rely on dimension-six squared contributions. It could be argued that dimension-8 contributions that interfere with the SM are of the same order in the EFT, so their inclusion might significantly affect our results. To illustrate this point, let us work in a specific example involving both dimension-6 and dimension-8 operators,

\[ \mathcal{L}_{\text{EFT}} \supset -\frac{4G_F}{\sqrt{2}} V_{ei} \left[ \xi_L^{(6)}(\bar{c}_{i}^L\gamma_{\mu}\nu_{\mu}^L)(\bar{e}_{L}\gamma_{\mu}d_{L}^i) - \frac{1}{M_{\text{NP}}} \xi_L^{(8)}(\bar{e}_{L}^i\gamma_{\mu}\nu_{\mu}^L)\partial^2(\bar{e}_{L}\gamma_{\mu}d_{L}^i) \right] + \text{h.c.}, \quad (4.7) \]

with the normalization chosen such that \( \xi_L^{(6,8)} \) are adimensional, and \( M_{\text{NP}} \) is the NP mass threshold. The corresponding partonic cross section including both SM and the EFT

\[ \alpha \]

\[ \epsilon \]

\[ \left[ \right. \]

\[ \left. \right] \]

\[ \times 10^2 \]

\[ \times 10^2 \]

\[ \times 10^3 \]
contributions in eq. (4.7) is given by

$$
\hat{\sigma}(s) = \frac{G_F^2 |V_{c1}|^2}{18\pi} s \left[ m_W^2 - \epsilon^{(6)}_{V_L} - \frac{s}{M^2_{NP}} \epsilon^{(8)}_{V_L} \right]^{2}
$$

$$
= \frac{G_F^2 |V_{c1}|^2}{18\pi} s \left[ \frac{m_W^2}{s^2} - 2 \frac{m_W^2}{s} \text{Re}(\epsilon^{(6)}_{V_L}) + |\epsilon^{(6)}_{V_L}|^2 - 2 \frac{m_W^2}{M^2_{NP}} \text{Re}(\epsilon^{(8)}_{V_L}) \right] + \mathcal{O}\left(\frac{1}{M^6_{NP}}\right),
$$

(4.8)

where, in the second line, we neglected the dimension-8 squared term. As already mentioned, the experimental limits in table 4 are dominated by the $|\epsilon^{(6)}_{V_L}|^2$ term, with a small correction from the term proportional to $\text{Re}(\epsilon^{(6)}_{V_L})$. The term proportional to $\text{Re}(\epsilon^{(8)}_{V_L})$ is even smaller than the dimension-6 interference if $|\text{Re}(\epsilon^{(8)}_{V_L})| \leq |\epsilon^{(6)}_{V_L}|$, since $M^2_{NP} > s$ by construction. To give an example of explicit UV realization, a single tree-level $s$-channel resonance exchange predicts $\epsilon^{(6)}_{V_L} = \epsilon^{(8)}_{V_L}$. A significant cancellation between dimension-6 and 8 contributions would require a peculiar NP scenario.

Another possible way to evade our limits within the SMEFT regime would consist in including a semileptonic operator mediating $u \bar{d} \rightarrow \bar{e} \nu \alpha$ transitions which negatively interferes with the dominant SM background. One could then enforce a tuning between NP contributions to reduce the number of NP events in the tails. Even with this tuning, the different $\sqrt{s}$ dependence of each contribution would not allow for an exact cancellation between the two.

The EFT is no longer valid if a new mass threshold is at or below the typical energy of the process. Indeed, inverting the obtained limits on the WCs ($v/\sqrt{s} \approx \text{few TeV}$) and invoking perturbative unitarity suggests that the largest scales currently probed are at most $\mathcal{O}(10 \text{ TeV})$ for strongly coupled theories. Any suppression in the matching, such as loop, weak coupling, or flavor spurion, brings the actual NP mass scale down. Clearly, the EFT approach has a significantly reduced scope in the high-$p_T$ lepton tails compared to charmed meson decays. Outside the EFT realm, one may wonder how well our limits approximate the correct values. Charged mediators responsible for generating charged currents at low energies, cannot be arbitrarily light since they would be directly produced at colliders by (at least) the EW pair production mechanism. Here, the signal yield is robustly determined in terms of the particle mass and known SM gauge couplings. A sizeable effect in low energy transitions also means sizeable decay branching ratio to usual final state with jets, leptons, etc, that has been searched for. Thus, charged mediators at or below the EW scale receive strong constraint from direct searches, yielding $M_{NP} \gtrsim \mathcal{O}(100 \text{ GeV})$.

One could think of possible mediators that satisfy this bound, but still have a mass within the energy range invalidating the SMEFT, since the energy in the high-$p_T$ tails is around the TeV. At tree-level, there are a finite number of possible mediators, either colorless $s$-channel or colored $t$ ($u$)-channel resonances. In the case of $s$-channel mediators, the high-$p_T$ limits derived in the EFT are overly conservative, due to the resonance enhancement (see e.g. figure 5 in [43]). On the other hand, for $t$ ($u$)-channel mediators, the EFT limits are typically (slightly) stronger than the real limits, but they serve as a good estimate (see e.g. figure 3 in [45]). In addition, these latter mediators, known as leptoquarks, are copiously produced at the LHC by QCD (see e.g. [101]), and direct exclusion limits push their
mass above the TeV. One could advocate for tuned scenarios where the high-$p_T$ contributions of a $t$-channel resonance is cancelled against a very wide $s$-channel resonance, while still yielding a sizable low-energy contribution (see example in section 6.1 of [102]). As in the previous case, this requires a tuning of the NP contributions, and one can only achieve a partial cancellation. Finally, loop-induced contributions require the NP scale to be significantly lower (or the NP couplings to be strong) in order to generate the same effects at low energies. This translates into typically stronger high-$p_T$ limits than the ones considered here, either from non-resonant or from resonant production of the new mediators.

As a final comment, the high-$p_T$ bounds estimated from the EFT approach are not expected to disappear outside the EFT validity range. This work then suggests that the high-$p_T$ analysis should be carefully done in an explicit new physics model of interest.

5 Interplay between low and high energy

Once we have clarified possible caveats concerning high-$p_T$ limits on effective operators we are ready to compare low and high-energy results and discuss their complementarity. The comparison for scalar and tensor operators is quite direct because they receive contributions only from four-fermion operators in the SMEFT, cf. eqs. (2.8). Vector and axial operators, on the other hand, receive two types of SMEFT contributions from: (i) four-fermion operators, and (ii) $W$ vertex corrections. As discussed in detail in section 4, only (i) experience the energy enhancement exploited by our analysis of the high-$p_T$ tails. In the following, we discuss the interplay between low-energy and high $p_T$ bounds in four-fermion operators and then we obtain limits on $W$ vertex corrections.

5.1 Four-fermion interactions

High-$p_T$ bounds on left-handed ($V - A$) four-fermion operators are almost an order of magnitude stronger than those derived from meson decays. In figure 2, we compare the regions excluded by charmed-meson decays (cf. table 2) and high-$p_T$ monolepton tails (cf. table 4) in the $(\epsilon^{V_{L\alpha\alpha}}_{\mu\mu}, \epsilon^{V_{L\alpha\alpha}}_{\tau\tau})$ plane, assuming NP only in the SMEFT operator $O_{lq}^{(3)}$. The three plots are for each lepton flavor conserving combination $\alpha = \beta$, while for $\alpha \neq \beta$ the improvement with respect to charm decays is even more significant. These comparisons provide a striking illustration of the LHC potential to probe new flavor violating interactions at high-$p_T$.

The high-$p_T$ LHC bounds are also stronger than those from $D_{(s)}$-meson decays in all channels and WCs except for the pseudoscalar operators, constrained by the electronic and muonic $D_{(s)}$ decays. As discussed in section 3 and shown in table 3, the latter strongly constrains any NP producing a single scalar or tensor operator at the high-energy scale. Even in this scenario, high-$p_T$ LHC limits are stronger for the tauonic operators and for the electronic tensor operators.

In NP scenarios where various operators with the same flavor entries are produced at the matching scale, the complementarity between high-$p_T$ LHC and meson decays becomes more pronounced. As discussed above, the quadratic contributions of NP dominate the high-$p_T$ limits, allowing one to extract bounds on several operators simultaneously (see e.g. figure 2). On the other hand, the $D_{(s)}$ branching fractions depend on interference.
Figure 2. Exclusion limits at 95% CL on $c \rightarrow d(\bar{s})\bar{e}^\alpha \nu^\alpha$ transitions in $(\epsilon_{V_L}^{ed}, \epsilon_{V_L}^{US})$ plane were $\alpha = e$ (top left), $\alpha = \mu$ (top right), and $\alpha = \tau$ (bottom). The region colored in pink is excluded by $D_{(s)}$ meson decays, while the region colored in blue is excluded by high-$p_T$ LHC.

terms between WCs, and some combinations remain unconstrained (tauonic operators) or poorly bounded by the low-energy data.

To illustrate this, we compare in figure 3 the constraints on the $(\epsilon_{S_L}^{\alpha\beta i}, \epsilon_{T}^{\alpha\beta j})$ planes for $\mu = 1$ TeV obtained from fits to low-energy and high-$p_T$ data. We also show projections for the HL-LHC (3 ab$^{-1}$) derived by rescaling the sensitivity of the corresponding monolepton expected limits with luminosity. The bound stemming from the leptonic decays can be clearly appreciated in these figures, while the orthogonal directions are only constrained at low-energies by the semileptonic decays (electron and muon) or remain unconstrained (tau). Also, as shown in figure 3, the low-energy bounds relax for LFV transitions as these do not interfere with the SM. For the same reason, imaginary WCs or operators beyond the SMEFT with light right-handed neutrinos accessible in charm decays are better constrained from high-$p_T$ tails.
Figure 3. 95% CL regions for the combined fits of $\epsilon_{\alpha \beta i}^{S_L}$ and $\epsilon_{T}^{\alpha \beta i}$ to the charmed-meson decay data with $\beta = \alpha$ (red solid line) or $\beta \neq \alpha$ (light-red dash-dotted line) and to monolepton LHC data (blue solid line). Projections for the high-luminosity phase of the LHC (3 ab$^{-1}$), obtained by rescaling the expected limits with luminosity, are represented by dashed ellipses.

5.2 W vertex corrections

Right-handed contributions of the type $\epsilon_{V R}^{\alpha i}$ can be generated at $\mathcal{O}(u^2/\Lambda^2)$ only as a vertex correction to the quarks by the operator $\mathcal{O}_{\phi ud}$ (universal for all lepton flavors $\alpha$). Thus, $\epsilon_{V R}^{\alpha i}$ does not receive a bound from our analysis of the LHC data. In case of the left-handed operator a combination of meson decay and high-$p_T$ LHC bounds constrains simultaneously vertex and four-fermion corrections. We define vertex corrections to $W$ couplings to quarks as

$$\mathcal{L}_W \supset \frac{g}{\sqrt{2}} V_{ci} \left( 1 + \delta g_{L}^{ci} \right) \bar{c} \gamma^\mu P_L d_i W^+_{\mu} + \frac{g}{\sqrt{2}} V_{ci} \delta g_{R}^{ci} \bar{c} \gamma^\mu P_R d_i W^+_{\mu} + \text{h.c.},$$

where in terms of the conventions of section 2 imply,

$$\delta g_{L}^{ci} = \frac{V_{ci}^{\dag} [C_{\phi q}]_{2j}}{V_{ci}^{\dag} [C_{\phi q}]_{2j}}, \quad \delta g_{R}^{ci} = \frac{1}{2 V_{ci}^{\dag}} [C_{\phi ud}]_{2i},$$

with a sum over $j$ implicit in the first equation. These coupling modifications are typically constrained by LEP and LHC on-shell vector boson production [103–105]. Still, our analysis of charm transitions can play an important role to fully constrain some of these couplings or give a handle to disentangle the contributions of different operators.

In table 5, we show the limits on the vertex corrections obtained by combining the low and high energy bounds in tables 2 and 4, respectively. The results for $\delta g_{L}^{ci}$ are obtained subtracting and profiling over the maximal contribution of four-fermion operators allowed by the high-$p_T$ tails. We have assumed that the analogous vertex corrections in the
couplings of the $W$ to the leptons are absent, so the bounds in the different channels can be combined (“Av.” in the table). In addition, for each lepton channel we are assuming that only one of the two possible corrections (left-handed or right-handed) are active at a time. This is not needed for the muon channels where leptonic and semileptonic decays lead to comparable limits such that both couplings can be simultaneously constrained. However for the electron (tau) channel only the bound from the semileptonic (leptonic) decay is relevant and there are blind directions in the corresponding ($\delta g^c_L$, $\delta g^c_R$) planes. It is remarkable that the combination of charm decays and high-$p_T$ monolepton tails leads to a determination of $W$ vertex corrections competitive to LEP and LHC on-shell $W$ production [103–105].

6 Neutral currents

6.1 Theoretical framework: $c \rightarrow u e^\alpha \bar{e}^\beta$

As a rule of thumb, flavor changing neutral currents (FCNC) probe scales far beyond the reach of current high energy colliders. However, FCNC in charmed meson decays seem to be an exception to a large extent. In this section, we perform a combined analysis of low- and high-$p_T$ data in the context of $c \rightarrow u e^\alpha \bar{e}^\beta$ transitions. The relevant dimension-six effective Lagrangian is

$$\mathcal{L}_{\text{NC}} = \frac{4G_F}{\sqrt{2}} \frac{\alpha}{4\pi} \sum_{k,\alpha,\beta} \epsilon^\alpha_\beta \mathcal{O}^\alpha_\beta + \text{h.c.} \quad (6.1)$$

The most general set of four-fermion operators compatible with $SU(3)_c \times U(1)_{\text{em}}$ is

$$\mathcal{O}^\alpha_\beta_{\text{LL}} = \bar{e}^\alpha_L \gamma^\mu e^\beta_L \overline{u}^\mu L \gamma^\alpha c_L,$$
$$\mathcal{O}^\alpha_\beta_{\text{LR}} = \bar{e}^\alpha_R \gamma^\mu e^\beta_L \overline{u}^\mu R \gamma^\alpha c_R,$$
$$\mathcal{O}^\alpha_\beta_{\text{RL}} = \bar{e}^\alpha_L \gamma^\mu e^\beta_R \overline{u}^\mu L \gamma^\alpha c_R,$$
$$\mathcal{O}^\alpha_\beta_{\text{RR}} = \bar{e}^\alpha_R \gamma^\mu e^\beta_R \overline{u}^\mu L \gamma^\alpha c_L,$$

$$\mathcal{O}^\alpha_\beta_{\text{T}L} = \bar{e}^\alpha_R \sigma^{\mu\nu} e^\beta_L \overline{u}^\mu R \gamma^\alpha c_L,$$
$$\mathcal{O}^\alpha_\beta_{\text{T}R} = \bar{e}^\alpha_L \sigma^{\mu\nu} e^\beta_R \overline{u}^\mu R \gamma^\alpha c_R,$$

$\alpha, \beta = 1, 2, 3$. The bounds on the effective operators are listed in Table 5.

Table 5. 95% CL limits on $Wcd_i$ vertex corrections assuming only one coupling active at a time. See section 5.2 for details.
with \(\alpha, \beta\) being lepton flavor indices. Note that mixed chirality tensor operators are zero by Lorentz invariance. The matching to the SMEFT in eq. (2.1) yields the following relations,

\[
\begin{align*}
\epsilon_{V_{LL}}^{\alpha\beta} &= \frac{2\pi}{\alpha\lambda_c} (|C_{ll}|_{\alpha\beta12} - |C_{ll}|_{\alpha\beta12}), \\
\epsilon_{V_{LR}}^{\alpha\beta} &= \frac{2\pi}{\alpha\lambda_c} |C_{lu}|_{\alpha\beta12}, \\
\epsilon_{S_{LL}}^{\alpha\beta} &= -\frac{2\pi}{\alpha\lambda_c} |C_{lequ}|_{\alpha121}, \\
\epsilon_{S_{LR}}^{\alpha\beta} &= 0, \\
\epsilon_{T_{L}}^{\alpha\beta} &= -\frac{2\pi}{\alpha\lambda_c} |C_{lequ}|_{\alpha21}, \\
\epsilon_{T_{R}}^{\alpha\beta} &= -\frac{2\pi}{\alpha\lambda_c} |C_{lequ}|_{\alpha121},
\end{align*}
\]

at the matching scale \(\mu = m_W\) and in the up-quark mass basis. We only consider the four-fermion operators in the Warsaw basis (see table 3 of ref. [52]) and neglect other effects such as the Z-boson vertex modification. The operators \(O_{S_{LL}}\) and \(O_{S_{RR}}\) are not generated in the SMEFT due to gauge invariance and are consistently neglected in our analysis. As discussed before, the RGE running from \(\mu = 1 \text{ TeV}\) down to \(\mu = 2 \text{ GeV}\) yields sizable effects in scalar and tensor operators, while the vector operators remain practically unchanged. In particular, using refs. [55, 57] we obtain

\[
\begin{align*}
\epsilon_{S_{X}}(2 \text{ GeV}) &\approx 2.1 \epsilon_{S_{X}}(\text{TeV}) - 0.5 \epsilon_{T_{X}}(\text{TeV}), \\
\epsilon_{T_{X}}(2 \text{ GeV}) &\approx 0.8 \epsilon_{T_{X}}(\text{TeV}),
\end{align*}
\]

where \(X\) stands for the same chirality pairs, either \(LL\) or \(RR\).

### 6.2 Rare charm decays

Short-distance SM contributions to \(c \rightarrow u\ell\ell^{(f)}\) transitions are strongly suppressed by the GIM mechanism. As a result, the main SM contributions to rare \(D\)-meson decay amplitudes are due to long-distance effects [17, 20, 22, 23, 106, 107]. While this will be a limiting factor once the experimental measurements become more precise, at present one can obtain bounds on short-distance NP entering in \(D^0 \rightarrow \ell\ell^{(f)}\) and \(D_{(s)} \rightarrow P\ell\ell^{(f)}\) by assuming that the experimental limits are saturated by short-distance NP contributions [20, 22, 23]. The short-distance contributions to the leptonic rare \(D\) decay rate read

\[
B(D^0 \rightarrow \ell_{a}^{+}\ell_{b}^{-}) = \frac{\tau_{D_{0}}}{256\pi^3} \frac{\alpha^2 G_F^2 F_D^2 \lambda^2}{m_{D_{0}}^2} \lambda^{1/2}(m_{D_{0}}^2, m_{\ell_{a}}^2, m_{\ell_{b}}^2)
\times \left\{ m_{D_{0}}^2 - (m_{\ell_{a}} + m_{\ell_{b}})^2 \right\} \left\{ (m_{\ell_{a}} + m_{\ell_{b}}) \epsilon_{A}^{\alpha\beta} - \frac{m_{D_{0}}^2}{m_{c} + m_{u}} \epsilon_{P}^{\alpha\beta} \right\}^2
+ \left\{ m_{D_{0}}^2 - (m_{\ell_{a}} + m_{\ell_{b}})^2 \right\} \left\{ (m_{\ell_{a}} - m_{\ell_{b}}) \epsilon_{A'}^{\alpha\beta} - \frac{m_{D_{0}}^2}{m_{c} + m_{u}} \epsilon_{P'}^{\alpha\beta} \right\}^2,
\]

with \(\lambda(a, b, c) = (a - b - c)^2 + 4bc\) and where we used the following WC redefinitions

\[
\epsilon_{A, A'}^{\alpha\beta} = (\epsilon_{V_{LR}}^{\alpha\beta} - \epsilon_{V_{LL}}^{\alpha\beta}) \mp (\epsilon_{V_{RR}}^{\alpha\beta} - \epsilon_{V_{RL}}^{\alpha\beta}), \quad \epsilon_{P, P'}^{\alpha\beta} = (\epsilon_{S_{LR}}^{\alpha\beta} - \epsilon_{S_{LL}}^{\alpha\beta}) \mp (\epsilon_{S_{RR}}^{\alpha\beta} - \epsilon_{S_{RL}}^{\alpha\beta}).
\]
As already discussed in section 3, leptonic decays are unable to probe parity-even scalar, vector and tensor quark currents. Moreover, axial vector quark currents are chirally suppressed. This suppression is particularly strong for the dielectron channel, making current limits from leptonic decays not competitive. In these cases, better limits are found using semileptonic transitions. The differential branching ratios for $D \rightarrow \pi \ell \ell^{(i)}$ and $D_s \rightarrow K \ell \ell^{(i)}$ decays are studied in refs. [20, 22]. Currently, the best limits are obtained using $D^+ \rightarrow \pi^+ \ell \ell^{(i)}$ decays, for which an expression analogous to that in eq. (3.2) can be found in ref. [22]. Barring cancellations among WCs, we derive the following 95% CL limits at the charm-mass scale:

$$
\begin{align*}
|\epsilon_{V_i}^{e}\epsilon_{eV_i}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 42, \\
|\epsilon_{S_{LL,RR}}^{e}\epsilon_{LL,RR}^{c}| & \lesssim 1.5, \\
|\epsilon_{T_{L,R}}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 66, \\
|\epsilon_{V_i}^{\mu}\epsilon_{\mu V_i}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 8, \\
|\epsilon_{S_{LL,RR}}^{\mu}\epsilon_{LL,RR}^{c}| & \lesssim 0.4, \\
|\epsilon_{T_{L,R}}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 9, \\
|\epsilon_{V_i}^{\mu,\mu}\epsilon_{\mu,\mu V_i}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 16, \\
|\epsilon_{S_{LL,RR}}^{\mu,\mu}\epsilon_{LL,RR}^{c}| & \lesssim 0.6, \\
|\epsilon_{T_{L,R}}^{c}\epsilon_{LL,RR}^{c}| & \lesssim 110,
\end{align*}
$$

(6.7)

with $i = LL, RR, LR, RL$. These low-energy limits have flat directions in WC space, which could significantly weaken these bounds in given NP scenarios. Moreover, there are no limits on tau leptons, since $D$ decays involving taus are either kinematically forbidden or have not been searched for like in the $D^0 \rightarrow e\tau$ case. In comparison with the light lepton case, the strong phase space suppression in $D^0 \rightarrow e\tau$ is compensated by the lack of chiral suppression for the axial current. If an experimental limit on the BR($D^0 \rightarrow e^{\pm}\tau^{\mp}$) at the level of the one for the BR($D^0 \rightarrow e^{\pm}\mu^{\mp}$) existed, we would obtain a bound of $|\epsilon_{V_i,LL,RR}^{e}\epsilon_{LL,RR}^{c}| \lesssim 10$.

Improvements on these bounds are expected from future measurements at LHCb [3], Belle II [4] and BESIII [2], although limitations to predict long-distance contributions will probably impact the reach that can be achieved. One remarkable exception is the branching fraction of the pure muonic decay $D^0 \rightarrow \mu^+\mu^-$. LHCb plans to improve the sensitivity to this observable by a factor $\sim 35$ reaching a value which still is significantly above the SM prediction [3]. Therefore, improvements on the sensitivity to $\epsilon_{A,PP}^{\mu,\mu}$ by a factor $\sim 6$ could be attained after HL-LHC. Furthermore, angular and CP asymmetries or lepton flavor universality tests in semileptonic decays of $D_{(s)}$ mesons (which can be measured at BESIII and Belle II) and $\Lambda_c$ baryons (accessible at LHCb) can be directly sensitive to

\footnote{Note that we use a different EFT basis compared to refs. [20, 22]. The relation between our WCs and those in this reference are

$$
C_{0,10} = \frac{\lambda_0}{2} (\epsilon_{V_LL}^{c_t} \pm \epsilon_{V_LL}), \quad C_{g,10} = \frac{\lambda_0}{2} (\epsilon_{V_{RR}}^{c_t} \pm \epsilon_{V_{LL}}), \quad C_{T,10} = \frac{\lambda_0}{2} (\epsilon_{T_L} \pm \epsilon_{T_L}),
$$

$$
C_{S,P} = \frac{\lambda_0}{2} (\epsilon_{SLL}^{c_t} \pm \epsilon_{SLL}), \quad C_{g',P} = \frac{\lambda_0}{2} (\epsilon_{SLL}^{c_t} \pm \epsilon_{SLL}).
$$

The SMEFT matching in eq. (6.3) imply $C_2 = C_P$ and $C_{g'} = -C_{g'}$. This is analogous to the relations for neutral currents in the down sector found in [108]. The main difference is that tensor operators are not generated in the down sector when matching to the SMEFT.

\footnote{For the $ee$ channel, we use the same hadronic coefficients as the ones provided in ref. [22] for the LFV case, given that both experimental limits are obtained from the same BaBar analysis [109] using the same kinematical regimes and that lepton mass effects are negligible.}}
### Table 6.

95% CL limits on the neutral-current WCs from $pp \to e^\alpha \bar{e}^\alpha$ at the LHC, with $i = LL, RR, LR, RL$. We also show in parenthesis the naive projections of the expected limits for the HL-LHC (3 ab$^{-1}$), assuming that the error will be statistically dominated.

| $\alpha$ | $|\epsilon_V^{\alpha\alpha}|$ (1 TeV) | $|\epsilon_{SLL,RR}^{\alpha\alpha}(\mu)|$ (2 GeV) | $|\epsilon_{TLL,RL}^{\alpha\alpha}(\mu)|$ (2 GeV) |
|---------|------------|-----------------|-----------------|
| $e$     | 13 (3.9)   | 15 (4.5)        | 32 (9.5)        |
| $\mu$   | 7.0 (3.4)  | 8.1 (3.9)       | 17 (8.3)        |
| $\tau$  | 25 (12)    | 29 (13)         | 60 (28)         |

short-distance contributions in $c \to u \ell \ell$, which could also improve the low-energy bounds in the future (see e.g. [22, 110]).

#### 6.3 High-$p_T$ dilepton tails

Following the footsteps of section 4 we perform the high-$p_T$ Drell-Yan analysis to extract the limits on the WCs. We focus on the lepton flavor conserving cases while the limits on LFV can be found in the recent ref. [48]. The partonic level cross section formula can be trivially obtained from eq. (4.2). The notable difference is that the SM contribution to $\bar{u}c \to e^\alpha \bar{e}^\alpha$ scattering is loop and GIM-suppressed. As a result, the interference of NP with the SM can be completely neglected. As discussed in section 4.1, the interference among different WCs is negligible for an inclusive angular analysis. These two statements have an important implication. Namely, the high-$p_T$ tails can set a bound on the sum of absolute values of WCs featuring different Lorentz structures.

We set up a simulation pipeline and analysis procedure analogous to the one discussed in section 4 to recast the experimental searches. For $ee$ and $\mu\mu$ channels, we recast the analysis from the CMS collaboration in ref. [111], using 140 fb$^{-1}$ of 13 TeV data. For the $\tau\tau$ channel, we use the search by ATLAS [112] with 36.1 fb$^{-1}$ of 13 TeV data. In all cases, we validate the simulation procedure against the MC samples for the SM $Z \to e^\alpha \bar{e}^\alpha$ process provided by the experimental collaborations. In $ee$ and $\mu\mu$ channels we achieved a 10% level of agreement with respect to the experimental results. For the $\tau\tau$ channel, we additionally validate our analysis against the CMS simulation of the sequential SM $Z'$ signal. In this case, the level of agreement achieved is around 20%. The 95% CL limits on the neutral-current WCs are shown in table 6. As in the charged-current case, these limits are provided both at the high-energy and at the low-energy scale, using the expressions in eq. (6.4).

As anticipated, the high-$p_T$ limits obtained for these transitions compete in most instances with those found at low-energies. This is particularly well illustrated in figure 4 for the vector operators. In this case, our high-$p_T$ limits are stronger than (comparable to) those obtained from low-energy data for the electron (muon) channel. For the tensor operators, high-$p_T$ offers a better probe, while the scalar operators are better constrained by leptonic charm decays, since they receive a large chiral enhancement in $D \to \ell^+\ell^-$ compared to the corresponding SM contribution. Let us also note that the limits from $e^+e^- \to jj$ from LEP-II are not competitive to the first row of table 6, see ref. [113].
Figure 4. Exclusion limits at 95\% CL on $c \to u \ell^+ \ell^-$ transitions in the $(\epsilon_{V_i}^{ee}, \epsilon_{V_i}^{\mu\mu})$ plane, where $i = LL, RR, LR, RL$. The region outside the red contour is excluded by $D$ meson decays, while the region outside the blue contour is excluded by high-$p_T$ LHC.

Furthermore, the $c \to u \tau^+ \tau^-$ transition is only accessible at high-$p_T$, since the corresponding low-energy decays are kinematically forbidden. Similar conclusions have been reached in the LFV channels \cite{48}. Namely, the high-$p_T$ bounds on the $\mu e$ channel are stronger than those from low-energy, with the exception of the scalar operators, while for $\tau e$ and $\tau \mu$ channels, high-$p_T$ tails offer the only available limits.

Concerning the possible caveats to the high-$p_T$ limits, there are two major differences with respect to the discussion for charge currents in section 4.3. Firstly, the $c \to u \ell^+ \ell^-$ SM amplitude is extremely suppressed, as mentioned before. Thus, the dimension-8 interference with the SM is negligible and unable to affect the leading dimension-6 squared contribution, even though the two are formally of the same order in the EFT expansion. Nonetheless, semileptonic operators with flavor-diagonal quark couplings which negatively interfere with the SM background can be used to tune a (partial) cancellation between NP contributions in the tails. Secondly, most UV completions of the relevant SMEFT operators feature mediators that are charged and (or) colored, such as leptoquarks or extra Higgses. The neutral components of these representations, which mediate $c \to u \ell^+ \ell^-$ transitions, cannot be significantly lighter than other SU(2)$_L$ components due to electroweak precision tests. As an exception, and unlike the charged-current case, it is now possible to have an $s$-channel tree-level mediator which is a complete SM gauge singlet, a vector $Z'$. Being a SM singlet, pair production limits are not robust and (a priori) the mediator could be very light. In this case, one would require a dedicated study for a low-mass dilepton resonance taking into account stringent limits from $D$ meson oscillation induced at tree-level.

As an illustration, let us provide an explicit model example for which our high-$p_T$ analysis provides a leading up-to-date constraint. We supplement the SM by a single scalar leptoquark with the SM quantum numbers $S_1 = (3, 1, 1/3)$, see ref. \cite{101}. 

\[ D \to \ell^+ \ell^+, \pi \ell^+ \ell^- \]
We also assume the dominate leptoquark interaction is with right-handed SM fermions, \( \mathcal{L} \supset y_{ij} \bar{u}^c_R \epsilon^R_i S_j + \text{h.c.} \), where \( y_{ij} \) is an arbitrary complex matrix in flavor space. The main effects of this model at low energies are (i) tree-level rare \( D \) meson decays and (ii) loop-level neutral \( D \) meson oscillations. As shown in ref. [22], the constraint from \( \Delta m_D \) amounts to
\[
|\sum_\ell y_{\ell c} y_{\ell u}^*| \leq 0.01 \frac{m_{LQ}}{\text{TeV}},
\]
where \( m_{LQ} \) is the leptoquark mass. This constraint is easily satisfied when \( y_{ij} \) is close to a unitary matrix. However, the high-\( p_T \) dilepton tails provide a competitive limit for each flavor separately, for example
\[
|y_{c\mu} y_{\mu u}^*| \leq 0.06 \left( \frac{m_{LQ}}{\text{TeV}} \right)^2.
\]
These are stronger than rare \( D \) meson decays for all lepton flavors. As we show in the supplemental material of ref. [45], the high-\( p_T \) analyses in the EFT and in the full leptoquark model agree well when \( m_{LQ} \gtrsim \text{TeV} \). This is also the mass range unconstrained by the leptoquark pair production, for a review see [101]. We note that TeV-scale leptoquarks are generically constrained by other low-energy probes, such as electric dipole moments, see e.g. refs. [114–116]. These however involve different combinations of couplings to what is probed by the high-\( p_T \) tails.

### 6.4 Comments on \( \Delta S = 1 \) and \( \Delta B = 1 \) rare transitions

In section 4, we showed how to translate the high-\( p_T \) monolepton bounds to other initial quark flavor combinations by simply rescaling with PDF, and validated this method against existing simulations of \( bc \rightarrow \tau \nu \). The reasoning behind this procedure is that the signal acceptance is similar for other initial quark combinations, since the analyses are largely inclusive in angular cuts and the invariant mass distributions have a similar shape across the small range of most sensitive bins in the tails. In analogy, the results of the high-\( p_T \) dilepton analysis reported in the context of \( \Delta C = 1 \) transitions in table 6 can be used to estimate the bounds on other flavor violating transitions.

To illustrate this point, here we constrain \( \Delta S = 1 \) and \( \Delta B = 1 \) rare transitions from high-\( p_T \) dilepton tails. More precisely, we derive limits on
\[
s \rightarrow d,
\]
\[
b \rightarrow d,
\]
and
\[
b \rightarrow s
\]
transitions starting from \( c \rightarrow u \) limits. The low-energy Lagrangian for \( d_i \rightarrow d_j \) with \( i > j \) is given by eqs. (6.1) and (6.2) after replacing \( \lambda_c \) with \( V_{ti} V_{tj}^* \), \( \bar{u} \) with \( \bar{d}_j \) and \( c \) with \( d_i \). Note that, tensor operators are absent for these transitions, see ref. [108] for the SMEFT matching in the down sector. By equating the hadronic cross sections in the tails, we find
\[
|\epsilon_{X}^{\alpha\beta j i} | = |\epsilon_{X}^{\alpha\beta uc} | \frac{\lambda_c}{|V_{ti} V_{tj}^*| \sqrt{L_{ij:cu}}},
\]
where
\[
L_{ij:cu} = \frac{\mathcal{L}_{d_i d_i} + \mathcal{L}_{d_j d_j}}{\mathcal{L}_{cu} + \mathcal{L}_{uc}}.
\]
The parton luminosity functions \( \mathcal{L}_{q \bar{q}} \) are defined in eq. (4.3) and evaluated in the most sensitive bin \( \sqrt{s} \sim [1–1.5] \text{TeV} \). The luminosity ratio \( L_{ij:cu} \) as a function of the dilepton invariant mass is shown in figure 5 for all \( i, j \) combinations. Some kinematic dependence is present when comparing valence and sea quarks, which limits the accuracy of the method to \( \mathcal{O}(10\%) \). Using eq. (6.8), we find approximate limits on the WCs of \( s \rightarrow d \), \( b \rightarrow d \), and \( b \rightarrow s \) to be 700, 40, and 20 times the \( c \rightarrow u \) limits in table 6, respectively.
Rare $\Delta S = 1$ and $\Delta B = 1$ decays to light leptons clearly outperform the high-$p_T$ searches. On the other hand, tauonic modes are difficult at low energies and experimental limits on e.g. $b \to s\tau^+\tau^-$ are far above the SM prediction, leaving plenty of room for NP. Assuming nonzero $\epsilon^{\tau\tau sb}_{V_{LL}} = \epsilon^{\tau\tau sb}_{V_{RL}}$, the BaBar search on $B \to K\tau^+\tau^-$ [117] imposes a limit $|\epsilon^{\tau\tau sb}_{V_{LL}}| < 990$ at 95% CL. However, this transition is better probed in $pp \to \tau^+\tau^-$ high invariant mass tail, $|\epsilon^{\tau\tau sb}_{V_{LL}}| < 420$. In addition, future prospects at the HL-LHC are more competitive than the prospects on $B \to K\tau^+\tau^-$ rescattering contribution to $B \to K\mu^+\mu^-$ derived in ref. [118].

Finally, a generic NP model correlates $\Delta F = 1$ operators to flavor non-universal flavor conserving $q^i\bar{q}^j \to e^\alpha\bar{e}^\alpha$ processes, which are the leading signatures if the flavor structure is MFV-like [42, 43]. In fact, in many explicit models, $b\bar{b} \to \tau^+\tau^-$ dominates over $V_{cb}$ suppressed $b\bar{s} \to \tau^+\tau^-$, see ref. [42].

7 Constraints from SU(2)$_L$ gauge invariance

Imposing SU(2)$_L$ gauge invariance yields strong constraints on the WCs entering in charm decays by relating them to other transitions, such as $K$, $\pi$ or $\tau$ decays. We discuss the impact of these correlated constraints here. To keep the SU(2)$_L$ relations as generic as possible, in this section we use a different flavor basis in which the SU(2)$_L$ doublets are defined as

$$ q^i_L = \begin{pmatrix} V_{ui}^* u^i_L \\ V_{di}^* d^i_L \end{pmatrix}, \quad t^\alpha_L = \begin{pmatrix} \nu_L^\alpha \\ e_L^\alpha \end{pmatrix}, \quad (7.1) $$

with the CKM matrix being $V = V_u^\dagger V_d$, while the right-handed fermions are already in their mass-eigenstate basis. Furthermore, whenever we do not impose down-quark alignment ($V_d \approx 1$) or up-quark alignment ($V_u \approx 1$) we assume that both $V_u$ and $V_d$ exhibit the same hierarchies as the CKM matrix.
7.1 Charged currents

We find the following complementary constraints:

- \( \mathcal{O}_{V_L}^{\alpha \beta i} \). We can decompose the SMEFT operators \( \mathcal{O}_{lq}^{(1,3)} \) as

\[
[\mathcal{O}_{lq}^{(1,3)}]_{\alpha \beta ij} = 2 (V_{ij}^{\alpha k} V_{ij}^{\beta l} [\mathcal{O}_{V_L}]^{\alpha \beta kl} + V_{ij}^{\alpha k} V_{ij}^{\beta l} [\mathcal{O}_{V_L}]^{\beta \alpha kl})
\]

\[
+ V_{ij}^{\alpha k} V_{ij}^{\beta l} \left[ (\bar{u}_L^{\alpha k} \gamma_\mu \nu_L^{\beta l}) (\bar{u}_L^{\alpha k} \gamma_\mu \nu_L^{\beta l}) - (\bar{e}_L^{\alpha k} \gamma_\mu e_L^{\beta l}) (\bar{e}_L^{\alpha k} \gamma_\mu e_L^{\beta l}) \right]
\]

\[
- V_{ij}^{\alpha k} V_{ij}^{\beta l} \left[ (\bar{d}_L^{\alpha k} \gamma_\mu d_L^{\beta l}) (\bar{d}_L^{\alpha k} \gamma_\mu d_L^{\beta l}) - (\bar{e}_L^{\alpha k} \gamma_\mu e_L^{\beta l}) (\bar{e}_L^{\alpha k} \gamma_\mu e_L^{\beta l}) \right],
\]

(7.2)

with \( \mathcal{O}_{V_L}^{\alpha \beta i} = \mathcal{O}_{V_L}^{\beta \alpha i} \). Clearly, by imposing SU(2)_L invariance, one obtains new operator structures that lead to additional observables. From eq. (7.2), we find correlated relations with the following observables:

i) Charged-current \( d_i \rightarrow u \ell \nu \) and \( \tau \rightarrow d_i \mu \nu \) transitions (1st line),

ii) Neutral-current \( c \rightarrow u \ell \ell (0), \tau \rightarrow \ell u u \) decays and \( \mu u \rightarrow e u \) conversion (2nd line),

iii) Neutral-current \( s \rightarrow d \ell \ell (0), s \rightarrow d \nu \nu, \tau \rightarrow \ell d d \) decays and \( \mu d_i \rightarrow e d_i \) conversion (3rd line),

where \( \ell = e, \mu \). Adjusting the coefficients of singlet and triplet operators in eqs. (7.2) and adopting up- or down-quark alignment, one can in principle avoid some of these correlations. However, one cannot always escape all of them simultaneously, as we will discuss in the following.

Assuming the CKM-like structure for \( V_{ud} \), \( K \rightarrow \pi \nu \nu \) decays impose \( |\epsilon_{V_L}^{\alpha \beta i}| \lesssim 10^{-4} \), independently of the quark and lepton flavors. These bounds are significantly stronger than both charm and high-pT limits (see sections 3 and 4.2). However, they can be alleviated by enforcing the relation \( C_{lq}^{(3)} \approx C_{lq}^{(1)} \), or by assuming down-alignment and a diagonal flavor structure (nonzero WCs only for \( i = j \)). Irrespective of these assumptions, the combination of \( K \rightarrow \pi \nu \nu, K_L \rightarrow e \mu \) and \( \mu - e \) conversion in nuclei set the robust bound \( |\epsilon_{V_L}^{\alpha \beta i}| \lesssim 10^{-4} \).

For the \( \tau \ell \) channel, LFV tau decays always offer bounds stronger than those from charm decays or high-pT. To alleviate these, together with those from \( K \rightarrow \pi \nu \nu \), one needs to enforce \( C_{lq}^{(3)} \approx -C_{lq}^{(1)} \) to cancel the contribution to tau decays plus the down-quark aligned flavor structure described above to avoid the bound from kaon decays. Even in that tuned scenario, the contribution to \( \tau \rightarrow \ell \rho \) remains unsuppressed, and the corresponding bounds are better than those from charm decays but comparable to the high-pT limits.

For the \( \ell \ell \) channel, the \( K \rightarrow \pi \nu \nu \) and \( K \rightarrow \ell \ell \) decays give the constraints \( |\epsilon_{V_L}^{\alpha \beta i}| \lesssim 10^{-3}, |\epsilon_{V_L}^{\alpha \beta i}| \lesssim 10^{-4} \), even if we allow for cancellations between the singlet and triplet operators.

For the \( c \rightarrow s \) case, it is possible to avoid these constraints by enforcing down alignment.
and a diagonal flavor structure with non-zero \( i = j = 2 \) entry. In this limit, the bounds from \( K \to \ell\nu \) are stronger than charged-current charm decays, and comparable to those from high-\( p_T \) monolepton tails. Likewise, for the \( c \to d \) decays obtained by demanding down alignment and a flavor structure with a non-zero \( i = j = 1 \) WC, one would enter in conflict with \( \pi \to \ell\nu \) decays or high \( p_T \) tails.

Finally, the only relevant neutral-current constraint for the \( \tau \tau \) channel is \( K \to \pi\nu\nu \), which can be removed by \( \mathcal{O}_{3}^{(3)} \approx \mathcal{O}_{3}^{(1)} \). Still, charged-current \( \tau \) decays provide comparable limits to those from charm decays, and can be alleviated with a mild alignment to the up eigenbasis.

\( \mathcal{O}_{SR}^{\alpha\beta i} \). The SMEFT operator \( \mathcal{O}_{ledq} \) decomposes as

\[
[O_{ledq}]^{\beta a ij} = V_u^{*} j k O_{SR}^{\alpha\beta k} + V_d^{*} j k (\bar{e}_R^a e_L^\beta) (d_R^i d_R^j), \tag{7.3}
\]

with \( O_{SR}^{\alpha\beta i} \approx O_{SR}^{\alpha\beta 2} \). Both LFV and lepton flavor conserving transitions involving first- and second-generation leptons are better probed in kaon decays than in charm decays. In general, the correlated neutral-current transitions \( K_L \to \ell^+\ell^- \) set constraints on the corresponding WCs that are orders of magnitude stronger. One can evade this bound by imposing a strong down-alignment. Even in this case, \( d_i \to u\ell\nu \) transitions provide stronger bounds than those from charged-current charm decays. Moving to \( \tau \), LFV combinations are better constrained by the correlated neutral-current \( \tau \to \ell P \) (\( P = K, \phi \)) decays. On the other hand, for \( \alpha = \beta = 3 \) no constraints from the neutral-current operators are obtained. However, for \( i = 2 \) the bounds from the charged-current \( \tau \to K\nu \) decays are stronger unless one imposes a mild alignment to the up basis.

\( \mathcal{O}_{SL}^{\alpha\beta i} \) and \( \mathcal{O}_{T}^{\alpha\beta i} \). We have the following decomposition for the SMEFT operators \( \mathcal{O}_{lequ}^{(1,3)} \):

\[
[O_{lequ}^{(1)}]^{\beta a 2} = V_{d}^{* k} \mathcal{O}_{SL}^{\alpha\beta k} + V_u^{* k} (\bar{e}^a_R e_L^\beta) (\bar{c}^k_R u^k_L), \tag{7.4}
\]

\[
[O_{lequ}^{(3)}]^{\beta a 2} = V_{d}^{* k} \mathcal{O}_{T}^{\alpha\beta k} + V_u^{* k} (\bar{e}^a_R \sigma_{\mu\nu} e_L^\beta) (\bar{c}^k_R \sigma_{\mu\nu} u^k_L),
\]

which yields additional operators that generically contribute to \( c \to u\ell\ell' \) transitions.

This is not relevant for transitions involving \( \tau \) leptons, since the bounds are absent due to kinematics. More precisely, \( c \to u\tau\tau \) and \( c \to u\mu\tau \) are forbidden while \( c \to u\ell\tau \) is suppressed. On the other hand, neutral-current charm decays provide stronger constraints than their charged-current counterpart for \( \alpha, \beta = 1, 2 \), unless the contributions to these transitions are suppressed by enforcing an approximate up alignment. While the scalar operators are better constrained at low energies for \( \alpha, \beta = 1, 2 \), the tensor operators receive more stringent bounds from high-\( p_T \). In this case, monolepton and dilepton bounds are comparable.

The interplay between charged-current charm decays, high-\( p_T \) lepton tails, and \( SU(2)_L \) relations is shown in figure 6 for \( \mu = 2 \text{ GeV} \). While it is possible to evade some of the constraints obtained by \( SU(2)_L \) gauge invariance, either by taking specific flavor structures and/or by having appropriate WC combinations, this typically requires tuning in
most UV completions. Moreover, the required conditions are not radiatively stable, and one should in general consider loop-induced misalignments in a given NP scenario. Going beyond this analysis, explicit models typically generate $\Delta F = 2$ transitions which are severely constrained by neutral meson oscillations. This can be particularly problematic in the context of the up alignment, and it represents a challenge for model building.

Another possible avenue beyond the SMEFT framework is to introduce a new light right-handed neutrino accessible in charm decays, yielding a new class of operators of the form $O_{\nu R} V_R = (\bar{e} R \gamma^\mu \nu R) (\bar{c} R \gamma^\mu d_i R)$. However, explicit UV completions of this operator are not completely free from $SU(2)_L$ relations (see refs. [53, 119]).

### 7.2 Neutral currents

Imposing $SU(2)_L$ gauge invariance in the neutral-current case also yields strong correlated constraints for the operators with left-handed fermions. Focusing on $O^{\alpha \beta}_{V_{LL}}$, it suffices to consider first only the contribution of the isosinglet SMEFT operator, $O^{(1)}_{lq}$, avoiding correlations with charged-current decays. Assuming the CKM-like structure for $V_d$ one obtains the limit $\epsilon^{\nu \beta}_{V_{LL}} < 0.2$ for any lepton flavor from $K_L \rightarrow \pi \nu \bar{\nu}$ decays. This bound, which is considerably stronger than those from neutral-current charm, can however be alleviated by enforcing down-quark alignment. Even in this case, the LFV combinations receive better constraints than those from neutral charm decays (or high-$p_T$ dilepton production) by using the correlated bounds from $\mu - e$ conversion in nuclei and LFV tau decays. On the other hand, charm decays and high-$p_T$ dilepton tails give stronger constraints for the lepton-
flavor conserving operators with $\alpha = \beta = 1, 2$ if down alignment is enforced. However, in models producing also the isorotplet SMEFT operator, $O_{lq}^{(3)}$, kaon semileptonic decays can provide similar (muon) or better (electron) bounds compared to charm rare decays.

Similarly, for the $O_{V_{RL}}^{\alpha \beta}$ operator, the correlated bounds from $\mu - e$ conversion and LFV tau decays offer the best limits for the LFV channels, independently of the quark flavor assumptions. For $\alpha = \beta = 1, 2$, the related limits from $K_L \to \ell^+ \ell^-$ yield bounds that are several orders of magnitude stronger than those from neutral charm decays, unless one imposes down alignment. On the other hand, the $\tau\tau$ channel remains unconstrained at low energies, even when considering the SU(2)$_L$ relations. Finally, no SU(2)$_L$ constraint can be derived for $O_{V_{LR}}^{\alpha \beta}$ since $D \to P \nu \bar{\nu}$ have not been searched for.

The $O_{S_{LL}}^{\alpha \beta}$ and $O_{T_{LL}}^{\alpha \beta}$ operators are related by SU(2)$_L$ invariance to $d_i \to u \ell \nu$ and $\tau \to ud \nu$ transitions. The ordering of indices in the chirality-flipping operator is relevant, since the second index refers to the left-handed lepton, and thus it is the one connected to the neutrino flavor. The related constraints are several orders of magnitude stronger than neutral charm for $O_{S_{LL}}^{\alpha}$, stronger than high-\text{p}_T dilepton tails for $O_{S_{LL}}^{\mu, \tau, \tau}$, and comparable to those from neutral charm for $O_{S_{LL}}^{\mu \nu}$. For $O_{T_{LL}}^{\alpha \beta}$, the SU(2)$_L$-correlated low-energy bounds are not competitive with the ones from high-\text{p}_T dilepton tails. However, the analysis of the high-\text{p}_T monolepton tails produced by $\bar{ud}_i \to e^\alpha \bar{\nu}^\beta$ give a marginal improvement compared to those. The $O_{S_{RR}}^{\alpha \beta}$ and $O_{T_{R}}^{\alpha \beta}$ operators receive correlated bounds from charged-current charm decays. These are only relevant for the lepton channels involving the tau flavor, since they are not constrained by the corresponding neutral currents. In this case, however, high-\text{p}_T dilepton production offers the best bounds, with the exception of $O_{S_{RR}}^{\tau \ell}$ that is better constrained by $D \to \ell \nu \tau$. The interplay between charm decays, high-\text{p}_T dilepton tails, and SU(2)$_L$ related constraints for the neutral-current case is summarized in figure 7 for $\mu = 2$ GeV.

8 Conclusions

Charm is a cornerstone of the SM; a unique arena for QCD and flavor, with a bright experimental future ahead. But how unique is the charm sector as a probe of new physics within the zoo of flavor and collider phenomenology? In other words, what is the role of charm in a broader quest for a microscopic theory beyond the SM?

In this work, we performed a detailed phenomenological analysis of new physics affecting charm $\Delta C = 1$ leptonic and semileptonic flavor transitions. We used effective field theory methods to establish a model-independent interplay between low- and high-energy experimental data, under the assumption of short-distance new-physics above the electroweak scale. The classic flavor-physics program consists in measuring and predicting the $D(s)$ meson decays with high precision. In the context of charged currents, we have focused on the pure leptonic decays $D(s) \to \ell \nu$ and the semileptonic decays $D \to P \ell \nu$ ($P = \pi, K$), for which accurate and robust predictions from lattice QCD exist and the most precise measurements have been reported. The main results are summarized in table 2, while the analogous limits on neutral currents are reported in section 6.2.
Figure 7. Interplay between charm physics, high-$p_T$, and SU(2)$_L$ relations for the neutral-current case ($\ell = e, \mu$ and $l = e, \mu, \tau$). The proximity of the WCs to a particular vertex of the triangle is determined, approximately, by the relative strength of the corresponding constraints. In purple, those constraints that can be avoided by a particular flavor structure and/or WC combination.

On the other hand, the analysis of high-$p_T$ lepton tails in $pp$ collisions at the LHC provides complementary constraints. Heavy flavors are virtually present in the proton and contribute to the Drell-Yan production with an amplitude which is connected by crossing symmetry to the one entering charmed meson decays. In fact, the energy-growing behavior of the EFT scattering amplitudes with respect to the SM, compensates for the lower partonic luminosities and lower statistics, eventually leading to strong constraints in the high-$p_T$ tails. The main results of our recast of recent ATLAS and CMS searches are reported in tables 4 and 6 for charged and neutral currents, respectively. A primary concern of the analysis is the EFT validity, discussed at length in section 4.3.

We find a striking complementarity between charm decays and high-$p_T$ lepton tails. The reason behind this is that QCD selects the parity basis of fermionic currents at low energy, while at high-$p_T$, chiral fermions act as independent asymptotic states. This is best illustrated for scalar and tensor operators, where the combination of the two datasets is crucial to set optimal constraints, see figure 3. For some scenarios, high-$p_T$ lepton tails offer the most competitive probe. As highlighted in figure 2, NP in four-fermion vector operators is by an order of magnitude better constrained in high-$p_T$ monolepton tails than in charm decays for all $c \to d\ell^+\ell^-$ transitions. Somewhat surprisingly, even for rare FCNC transitions $c \to u\ell^+\ell^-$, we find $pp \to \ell^+\ell^-$ high invariant mass tails to compete well with $D \to \ell^+\ell^-$, see figure 4. The results presented here are applicable even beyond charm physics. In particular, in section 6.4 we reinterpret the high-$p_T$ analysis in terms of
limits on $b \to s\tau^+\tau^-$ transitions to show that these are more stringent that the ones from $B \to K\tau^+\tau^-$ searches.

Embedding the low energy effective theory in the SU(2)$_L \times$ U(1)$_Y$ gauge invariant SMEFT, implies powerful model-independent correlations among observables in different sectors. Specific connections usually require to select a specific set of operators and its flavor structure as a remnant of a particular class of dynamics and symmetries in the UV. Nonetheless, one can assess the level of tuning required to avoid certain constraints or even find that avoiding all of them is not possible. An exhaustive map of SU(2)$_L$ correlations of charm decays with $K$, $\tau$ and $\pi$ decays is presented in section 7, see also figures 6 and 7. In conclusion, and to answer the question posed in the first paragraph of this section, the bounds from $D(s)$ decays, high-$p_T$ lepton tails and SU(2) relations chart the space of all SMEFT operators affecting semi(leptonic) charm flavor transitions.

Acknowledgments

We thank Nudžem Selimović for carefully reading the manuscript. The work of JFM has received funding from the Swiss National Science Foundation (SNF) under contract 200021-175940, and from the Generalitat Valenciana under contract SEJI/2018/033. The work of JFM and AG is partially supported by the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme, grant agreement 833280 (FLAY). JMC acknowledges support from the Spanish MINECO through the “Ramón y Cajal” program RYC-2016-20672 and the grant PGC2018-102016-A-I00. J.D.R.-Á. gratefully acknowledges the support of the Colombian Science Ministry and Sostenibilidad-UdeA.

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