Study of Some Agricultural Crop Production Planning Condition through Fuzzy Multi-Objective Linear Programming Mathematical Model

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Abstract: Present study is an application of fuzzy optimization technique in agricultural planning particularly for farmers of Patan district, North Gujarat, India. Generally the crop planning problem is formulated as linear programming problem but in real situation there are many uncertain factors in agricultural production planning problems. Therefore future profit for crops is imprecise and uncertain. In this article an attempt is made to formulate a model for crop planning.

Keywords: Agricultural crops, Fuzzy Multi-Objective linear programming mathematical Model, Patan district

1. Introduction

Agriculture plays vital role in the Indian economy. India’s geographical condition is unique for agriculture because it provides many favorable conditions. There are plain areas, fertile soil, long growing season and wide variation in climatic condition. Apart from unique geographical conditions, India has been consistently making innovative efforts by using science and technology to increase production. In agricultural production planning problems major objective is to maximize the profit under the minimum investment with some other constraints. An important issue in this problems is to optimize the objectives, based on one or multi-objective optimization, one or more goal to be considered. These problems of allocation of land for different crops, maximization of production of crops, maximization of profit are addressed in agricultural management system. Maximization of crop production can’t guarantee the maximization of profit. Profit or loss is also depending on fluctuating demand and cost for the particular crop. Also agriculture is a process that, at any moment of time associated with the issue of risk, and there is no certainty. So the maximization of profit turns out to be fuzzy multi-objective decision making problem.

2. Literature Review

Fuzzy mathematical programming has been investigated and developed in several research studies. One of the important early contributions in fuzzy programming was given by Zimmermann [1] and [2]. In fuzzy multi-objective programming, Sakawa et al. [3] have presented an interactive fuzzy approach for multi-objective linear programming problems. One of the main approaches in dealing with fuzzy models is the possibility theory. The basic work in possibility theory was introduced by Dubois and Prade [4]. Their work has presented the foundation of the possibility programming approach, which has been applied to fuzzy linear single objective and multiobjective programming [5] and [6].

For agricultural production where uncertainty and vagueness effect the profit directly or indirectly, several researchers such as Slowinski [4], Sinha et al.[5], Sher and Amir[6], Samps et al [7], Saraker et al[8], Pal and Moitra [9], Vasant [10], Biswas and Pal [11] used fuzzy goal programming techniques for farm planning problems. Lodwick et al. [12] made a comparison of fuzzy stochastic and deterministic method in a case of crop planning problem followed by a study of Itoh and Ishii [14] based on possibility measure. Itoh et al. [13] considered a problem of crop planning under uncertainty assuming profit coefficients are discrete random variables and proposed a model to obtain a maximum and minimum value of gains for decision maker. Sakawa and Yano[16], Chanas[17] used various types of membership functions for obtaining compromise solution. Anjali Garg, Shiva Raj Singh[15] provided a procedure to solve MOLP using Max Min approach to build up the member ship function and stated that it provides superior results.

3. Study Area

Patan district is located at 20°41’ to 23°55’ North Latitude and 71°31’ to 72°20’ East Latitude in western India. Patan district is surrounded by Banaskantha District, Desert of Kutch, some part of Surendranagar District and Mahesana District.

Total geographical area of the district is about 5.66 lakhs hectares. 70% of the geographical area is under cultivation in the district. Economy of the district mainly depends on agriculture, as 63.9 percent workers are engaged in primary sector. Net sown area of the district is about 3.93 lakh hectare and gross sown area is about 4.86 lakh hectares. The major crops cultivated in the district are castor, mustard and cotton. Also other crops grown are cumin, bajara, wheat, juwar and fennel. In some areas pulses like mung, tur, gram and vegetables are cultivated in the district. Depletion of water table, Deterioration of soil and water conditions due to salinity ingress, irregularity of rainfall, recurrent droughts/scarcity is the major factors that have impeded agricultural productivity in the Patan district. The purpose of applying
the techniques discussed in this paper is to achieve the best model for crop cultivation planning.

4. Methodology

First we introduce basic terms and definitions related to the paper and then mathematical formulation of the problems and finally the conclusion of the studies

1) Multi Objective linear programming problem: In general, a multi objective optimization problem with k objectives, n variables and p constraints is as:

Max \{Z_1, Z_2, ..., Z_k\}  
Such that:  
\text{subject to}  
A_j x \leq b_j  \quad j = 1, 2, \ldots, p \quad x_i \geq 0, \quad i = 1, 2, \ldots, n

2) Fuzzy Multi Objective linear programming problem:

Max Z_1(x) = \sum_{i=1}^{n} C_{1i} x_i  
Max Z_2(x) = \sum_{i=1}^{n} C_{2i} x_i

Subject to:  
x \in X \subseteq \mathbb{R}^n \land A_j x \leq b_j  \quad j = 1, 2, \ldots, p \quad x_i \geq 0, \quad i = 1, 2, \ldots, n

Where x is a n-dimensional vector of decision variable.  
Z_1(x), Z_2(x), ..., Z_k(x) are p distinct linear objective functions of the decision variable x

C_{ij} is the cost factor vector,  
i = 1, 2, ..., m  
j = 1, 2, ..., n

subject to x \in X \subseteq \mathbb{R}^n \land A_j x \leq b_j  \quad j = 1, 2, \ldots, p \quad x_i \geq 0, \quad i = 1, 2, \ldots, n

Now transform multiobjective linear programming problem into linear programming problem as Max \gamma

\mu_p(x) = \frac{Z_p(x) - Z_p^*}{Z_p^* - Z_p} \geq \gamma, \quad x \in X

Where \mu_p(x) = \sum_{i=1}^{n} C_{pi} x_i \quad 0 \leq \gamma \leq 1

such that:  
\mu_p(x) \geq \gamma, \quad x \in X

Here membership functions of objective function is estimated by obtaining pay off matrix of positive ideal solution and assume that membership functions are of the type non decreasing linear or hyperbolic etc.

Algorithm

In this section, by using of fuzzy multi objective linear programming approach, computational algorithm for a scenario when production co-efficient are crisp discrete random variables given. There are three important seasons namely kharif starting from June ending with October-November, Rabi season starting from November ending with February-March & Summer season starting March ending with May. For the present study the data has been collected from the department of statistics and economics, revenue etc. and presented as revenue per unit yield of crop, Investment input cost per unit yield of crop, Yield of i\textsuperscript{th} crop per unit land, Total irrigated land, Total cultivated land, Total availability of water, Maximum possible yield of all crops etc. The data from above source also gives us cost on seeds for i\textsuperscript{th} crop per unit area of land, cost on fertilizers for i\textsuperscript{th} crop per unit area of land, cost on pesticides for i\textsuperscript{th} crop per unit area of land, cost on Human power for i\textsuperscript{th} crop per unit area of land, cost on Animal & Other labor for i\textsuperscript{th} crop per unit area of land, cost on Cash rent for i\textsuperscript{th} crop per unit area of land, cost on Unforeseen expenditure for i\textsuperscript{th} crop per unit area of land, cost on Gross inputs for i\textsuperscript{th} crop per hectare of land etc. along with their total possible investment of cost. The raw data requires formatting for identification of inputs and the raw statistical data as per the requirements to be incorporated as inputs. After formatting the statistical data we have run the optimal programming problem on LINDO61 software. We have obtained the optimal section of decision variables on two accounts for obtaining (1) Maximum Production (2) Maximum Profit. The outputs were analyzed with suitable statistical graphs and are placed below.

Step 1: Solve the one objective function with constraint at time t, using linear programming techniques & then step by step find the corresponding value of all the objective functions for each of solutions.

Step 2: Then find lower bound Z_p and upper bound Z_p for each objective functions.

Let \mu_p be a linear non decreasing membership function between Z_p and Z_p, for\forall p.

Where \mu_p(x) = \begin{cases} \frac{1}{Z_p(x) - Z_p^*} & \text{if } Z_p(x) = Z_p^* \\ \frac{Z_p(x) - Z_p^*}{Z_p^* - Z_p} & \text{if } Z_p^* \leq Z_p(x) \leq Z_p^* \\ \frac{Z_p(x) - Z_p^*}{Z_p^* - Z_p} & \text{if } Z_p(x) < Z_p^* \end{cases}

Step 3: Now transform multiobjective linear programming problem into linear programming problem as Max \gamma

\mu_p(x) = \frac{Z_p(x) - Z_p^*}{Z_p^* - Z_p} \geq \gamma, \quad x \in X

Where Z_p(x) = \sum_{i=1}^{n} C_{pi} x_i \quad 0 \leq \gamma \leq 1

such that:  
\mu_p(x) \geq \gamma, \quad x \in X

It can easily solve by two phase simplex method.

Mathematical formulation of crop production problem

The objectives of the problem are to maximize the production and profit .The computational algorithm developed above is implemented step by step to find a optimal solution of crop production for Patan district, Gujarat. In this district farmers grow Cotton, Mung, Udad, Sesamum, Bajra in kharif season, Bajara in summer season. Gram, Wheat, Mustard, Castor, Fennel, Cumin, Tur, Potato in rabi season. The land available is 392669 hectare with given labour hours constrains. The labour availability for each season is given to be 220 total mandays. A small farm

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holder needs at least 400 kg of wheat, 200 kg of Bajara and 40 kg of Mung for his annual food grains requirement. The problem of the framer is to plan a suitable crop combination for his land to get maximum profit and aspiration level of rupees 175000 is set to meet his other annual family requirement. The objectives of the problems are to maximize profit and production to provide minimum food grain requirement.

Profit problem of the framer is to plan a suitable crop combination for his land to get maximum profit and aspiration level of rupees 175000 is set to meet his other annual family requirement. The objectives of the problems are to maximize profit and production to provide minimum food grain requirement.

Profit \( Z_2 \) = 235760 Rs.
Similar process is applied for objective function \( Z_2 \).

Profit \( Z_2 = 484071 \) Rs.

Positive Ideal Solution:

| \( Z_1 \) | \( Z_2 \) |
|---|---|
| 81186 | 235760 | 248071 |

The problem is converted into following form (by step: 3) 
Maximize \( \gamma \)

Such that

**Labour:**

189\( x_{1,1} \) + 39\( x_{1,2} \) + 30\( x_{1,3} \) + 40\( x_{1,4} \) + 68\( x_{1,5} \) \( \leq 220 \)
310\( x_{2,1} \) + 288\( x_{2,2} \) + 74\( x_{2,3} \) + 63\( x_{2,4} \) + 57\( x_{2,5} \) + 110\( x_{2,6} \) + 13\( x_{2,7} \) + 71\( x_{2,8} \) \( \leq 220 \)

76\( x_{3,1} \) \( \leq 220 \)

**Land:**

\( x_{1,1} + x_{1,2} + x_{1,3} + x_{1,4} + x_{1,5} \leq 392669 \)
\( x_{2,1} + x_{2,2} + x_{2,3} + x_{2,4} + x_{2,5} + x_{2,6} + x_{2,7} + x_{2,8} \leq 392669 \)
\( x_{3,1} \leq 392669 \)

**Food requirements:**

3238\( x_{2,2} \) \( \geq 400 \)
497\( x_{1,5} \) + 2563\( x_{3,1} \) \( \geq 200 \)
481\( x_{1,2} \) \( \geq 40 \)

Where \( x_{ij} \) is the area for cultivation of crop \( j \) in
Season \( i = 1, 2, 3 \) (heaters)
\( i = 1 \) = kharif season, \( i = 2 \) = Rabi season,
\( i = 3 \) = summer season

The objective functions are:

**Production:**

Maximize \( Z_1 = 992x_{1,1} + 481x_{1,2} + 745x_{1,3} + 421x_{1,4} + 497x_{1,5} + 698x_{2,1} + 3238x_{2,2} + 1562x_{2,3} + 1854x_{2,4} + 1358x_{2,5} + 441x_{2,6} + 985x_{2,7} + 23281x_{2,8} + 2563x_{3,1} \)

**Profit:**

Maximize \( Z_2 = 32119x_{1,1} + 5894x_{1,2} + 2964x_{1,3} + 6948x_{1,4} + 2985x_{1,5} + 1093x_{2,1} + 18418x_{2,2} + 7485x_{2,3} + 61067x_{2,4} + 36633x_{2,5} + 4046x_{2,6} + 66853x_{2,8} + 5066x_{3,1} \)

Subject to constraints:

**Labour:**

189\( x_{1,1} \) + 39\( x_{1,2} \) + 30\( x_{1,3} \) + 40\( x_{1,4} \) + 68\( x_{1,5} \) \( \leq 220 \)
310\( x_{2,1} \) + 88\( x_{2,2} \) + 74\( x_{2,3} \) + 63\( x_{2,4} \) + 57\( x_{2,5} \) + 110\( x_{2,6} \) + 13\( x_{2,7} \) + 71\( x_{2,8} \) \( \leq 220 \)

76\( x_{3,1} \) \( \leq 220 \)

**Land:**

\( x_{1,1} + x_{1,2} + x_{1,3} + x_{1,4} + x_{1,5} \leq 392669 \)
\( x_{2,1} + x_{2,2} + x_{2,3} + x_{2,4} + x_{2,5} + x_{2,6} + x_{2,7} + x_{2,8} \leq 392669 \)
\( x_{3,1} \leq 392669 \)

**Food requirements:**

3238\( x_{2,2} \) \( \geq 400 \)
497\( x_{1,5} \) + 2563\( x_{3,1} \) \( \geq 200 \)
481\( x_{1,2} \) \( \geq 40 \)

Where all \( x_{ij} \geq 0, i = 1, 2, 3 \& j = 1 \) to 8

Solve this linear programming problem by simplex method for objective function \( Z_1 \).

Production \( Z_1 = 81186 \) kg.
Production \( Z_2 = 48567 \) kg
Profit \( Z_2 = 362020 \) Rs.
5. Discussion

The present study shows that, marginal farmholders can get 3466 kg to 23834 kg production, small farm holders can get 3743 kg to 30807 kg, production, semi medium farm holders can get 88888kg to 51527 kg, production, medium farm holders can get 17572 kg to 90528 kg. Production & large farm holders can get 274383 kg and above crop production of various crops during whole year.

In Patan district, most of farmers are semi middle and middle farm holders. On the other hand land constraints has a very important role in determining the optimal model. According to results farmer can get profit of Rs.362020 which is more than his aspiration level. Also a farmer can achieve maximum production and plan his course of action on multiobjective task. The application of fuzzy concept in cropping pattern for high economic expectations has successfully tackled the uncertainty and imprecision in profits and production.

References

[1] H. J. Zimmermann, “Fuzzy programming and linear programming with several objective functions”, Fuzzy Sets and Systems, 1(1978), pp. 45-55.
[2] H. J. Zimmermann, “Fuzzy mathematical programming”, Computers and Operations Research, 10 (1983), pp. 291–298.
[3] M. Sakawa, H. Yano, T. Yumine, “An interactive fuzzy satisficing method for multiobjective linear-programming problems and its Application” IEEE Transactions on Systems, Man, and Cybernetics, 17 (1987), pp. 654–661.
[4] R. Słowinski, “A multi criteria fuzzy linear programming method for water supply system development planning”, Fuzzy Sets and Systems, 19 (1986), pp. 217-237.
[5] S. B. Sinha, K. A. Rao, and B. K. Mangaraj, “Fuzzy goal programming in multicriteria decision systems- A case study in agriculture planning”, Socio –Economic Planning Sciences, 22(2) (1988), pp. 93-101.
[6] A. sher and I. Amir, “Optimization with fuzzy constraints in agriculture production planning”, Agricultural systems. 45 (1994), pp. 421-441.
[7] J. M. Sumpsi, Francisco Amador, Carlos Romero, “On farmer’s objectives: A multi criteria approach”, European Journal Of Operation Research. 96(1996), pp. 64-71.
[8] R. A. Sarker, S. Talukdar and A. F. M. Anwarul Haque, “Determination of optimum crop mix for crop cultivation in Bangladesh”, Applied Mathematical Modelling, 21(1997), pp. 621-632.
[9] B. B. PAL, B. M. Moitra, “Fuzzy goal programming approach to long term land allocation planning in agricultural system: A case study”, Proceedings of fifth international conference on Advances in pattern recognition, Allied publishers Pvt. Ltd.(2003), pp.441-447.
[10] P. M. Vasant, “Application of fuzzy linear programming in production planning”, Fuzzy Optimization and Decision Making, 3(2003), pp. 45-55.
[11] A. Biswas, B. B. Pal, “Application of fuzzy goal programming technique to land use planning in agricultural system”, Omega, 33(2005), pp. 391-398.
[12] W. Lodwick, D. Jamison and S. Russell, “A comparison of fuzzy stochastic deterministic methods in linear programming”, Proceeding of IEEE, (2000), pp. 321-325.
[13] T. Itoh, H. Ishii, T. Nanseki, “Amodel of crop planning under uncertainty in agriculture management”, Int J. Production Economics, 81-82(2003), pp. 555-558.
[14] T. Toyonaga, T. Itoh, H. I shii, “A crop planning problem with fuzzy random profit coefficients”, Fuzzy Optimization and Decision Making, 4(2005), pp.51-59.
[15] A. Garg, S. R. Sinh, “Optimization under uncertainty in agricultural production planning”, I concept pocket journal: Computational Intelligence for Financial Engineers, 1(2010), pp. 1-12.
[16] M. Sakawa and H.Yano, “Interactive fuzzy decision making for multiobjective nonlinear programming using augmented minimax problems”, Fuzzy Sets and Systems, 20(1986), pp.31-43.
[17] S. Chanas, “Fuzzy programming in multiobjective linear programming-A parametric approach”, Fuzzy Sets and Systems, 29(1989), pp.303-313.

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| Season | Farmsize in Crop ha. | Marginal | Semi Medium | Medium | Large |
|--------|---------------------|----------|-------------|--------|-------|
|        | Below 1.0 | 1.0 to 9.9 | 2.0 to 29.9 | 3.0 to 39.9 | 4.0 to 49.9 | 5.0 to 79.9 | 7.5 to 99.9 | 10.0 to 119.9 | 12 & above |
| Kharif | Mun | 0.083160 | 0.083160 | 0.083160 | 0.083160 | 0.083160 | 0.083160 | 0.083160 | 0.083160 | 0.083160 |
|        | Sesamum | 0.2660.96 | 0.92 to 9.1 | 1.92 to 9.1 | 3.92 to 9.1 | 4.92 to 9.1 | 7.92 to 9.1 | 9.92 to 9.1 | 11.92 & above |
|        | Wheat | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 |
|        | Fennel | 0.2660.88 | 0.88 to 8.7 | 1.88 to 8.7 | 3.88 to 8.7 | 4.88 to 8.7 | 7.88 to 8.7 | 9.88 to 8.7 | 11.88 & above |
| Rabi   | Wheat | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 |
|        | Fennel | 0.2528802 | 0.5 to 5.0 | 1.5 to 5.0 | 3.5 to 5.0 | 4.5 to 5.0 | 7.5 to 5.0 | 9.5 to 5.0 | 11.5 & above |
|        | Potato | 0.3505868 | 0.40 to 0.8 | 1.40 to 0.8 | 3.40 to 0.8 | 4.40 to 0.8 | 7.40 to 0.8 | 9.40 to 0.8 | 11.4 & above |
| Summer | Wheat | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 | 0.123533 |
|        | Fennel | 0.2528802 | 0.5 to 5.0 | 1.5 to 5.0 | 3.5 to 5.0 | 4.5 to 5.0 | 7.5 to 5.0 | 9.5 to 5.0 | 11.5 & above |
|        | Potato | 0.3505868 | 0.40 to 0.8 | 1.40 to 0.8 | 3.40 to 0.8 | 4.40 to 0.8 | 7.40 to 0.8 | 9.40 to 0.8 | 11.4 & above |