Anisotropic optical properties induced by uniaxial strain of monolayer C\textsubscript{3}N: a first-principles study\textsuperscript{†}

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The optical properties, structural properties and electronic properties of a new two-dimensional (2D) monolayer C\textsubscript{3}N under different strains are studied in this paper by using first-principles calculations. The applied strain includes in-layer biaxial strain and uniaxial strain. The monolayer C\textsubscript{3}N is composed of a number of hexagonal C rings with N atoms connecting them. It is a stable indirect band gap 2D semiconductor when the strain is 0\%. It could maintain indirect semiconductive character under different biaxial and uniaxial strains from $\varepsilon = -10\%$ to $\varepsilon = 10\%$. As for its optical properties, when the uniaxial strain is applied, the absorption and reflectivity along the armchair and zigzag directions exhibit an anisotropic property. However, an isotropic property is presented when the biaxial strain is applied. Most importantly, both uniaxial tensile strain and biaxial tensile strain could cause the high absorption coefficient of monolayer C\textsubscript{3}N to be in the deep ultraviolet region. This study implies that strain engineering is an effective approach to alter the electronic and optical properties of monolayer C\textsubscript{3}N. We suggest that monolayer C\textsubscript{3}N could be suitable for applications in optoelectronics and nanoelectronics.

1 Introduction

Two-dimensional materials have attracted many scientists’ attention due to their novel properties which are different from those of their bulk counterparts.\textsuperscript{1–5} As is well known, two-dimensional materials have distinct electronic and structural properties, which can be used for novel nanoelectronic devices.\textsuperscript{6–7} For example, many researchers made use of the attractive electronic and carrier transition properties exhibited by graphene and applied it to transistors, supercapacitors, and gas sensor devices.\textsuperscript{8–11} However, there are only limited studies on graphene being used for the high-performance field effect in transistors and logic circuits due to its lack of a band gap.\textsuperscript{12–13} In addition, 2D MoS\textsubscript{2} and some other transition metal dichalcogenide (TMD) compounds are treated as promising materials as they show a finite band gap and other intriguing electronic properties which differ from those of graphene.\textsuperscript{14–18} And these TMD materials were shown to be used as gas sensors. Nevertheless, their carrier mobilities cannot compete with that of graphene and tend to be strongly affected by physical and chemical adsorbates. Recently, 2D black phosphorene has attracted increasing attention due to its high stability and carrier mobility,\textsuperscript{19–21} which makes 2D BP as a promising application for nanoelectronics and optoelectronics.\textsuperscript{22–24} However, 2D BP shows a weakness in its structural stability.\textsuperscript{19,20} Consequently, it is very important to find the novel two-dimensional layered nanostructures with moderate band gap and good structural stability.

Lately, scientists have synthesized 2D C\textsubscript{3}N by pyrolysing the hexaaminobenzene (HAB) trihydrochloride single crystals, and characterizing it through STM and STS.\textsuperscript{13} In 2016, Ke et al. have successfully synthesized monolayer C\textsubscript{3}N.\textsuperscript{25} Besides, the thermal stability of at high temperature monolayer C\textsubscript{3}N has been studied by first-principle calculation.\textsuperscript{19} Owing to its outstanding properties, 2D C\textsubscript{3}N is expected to be used for novel nanoelectronic devices.\textsuperscript{26–28} However, for the monolayer C\textsubscript{3}N, strain-tunable optical properties is not complete. For these reasons, we have developed a keen interest in the strain effect on optical and electronic properties of monolayer C\textsubscript{3}N.

In this study, the changing trends of strain engineering on optical properties, structural properties and electronic properties of a new two-dimensional (2D) monolayer C\textsubscript{3}N are calculated by using first-principles calculations. The PBE method is used to calculate the electronic and optical properties, and the hybrid functional HSE06 method is used to further modify the band gap and optical absorption edge. The studied strain includes in-layer biaxial strain and uniaxial strain. We find that the monolayer C\textsubscript{3}N presents a stable indirect band gap 2D semiconductor when the strain is 0\%. In addition, monolayer C\textsubscript{3}N represent indirect semiconductive characters under different biaxial and uniaxial strain from $\varepsilon = -10\%$ to $\varepsilon = 10\%$. The monolayer C\textsubscript{3}N can be treated as a series of hexagonal C...
rings with the connections of N atoms. Interestingly, as for the optical property, the absorption and reflectivity properties along armchair and zigzag directions exhibit anisotropic property when we applied uniaxial strain. However, when we applied biaxial strain, the absorption and reflectivity properties along armchair and zigzag directions show isotropic property. Moreover, uniaxial tensile strain and biaxial tensile strain could cause the high absorption coefficient of monolayer C$_3$N in the deep ultraviolet region. Furthermore, we explored the structural properties and electronic properties when in-layer uniaxial strain and biaxial strain are applied respectively. This study implies that the strain engineering is effective tunable approaches to alter the electronic and optical properties of monolayer C$_3$N. Namely we suggest that monolayer C$_3$N could be suitable for the applications in optoelectronics and nanoelectronics.

2 Simulation details (method)

Our calculations were performed using the Vienna ab initio simulation package (VASP)\textsuperscript{26–29} with the projector augmented wave (PAW)\textsuperscript{30} pseudopotentials.\textsuperscript{28,29} We used the Perdew-Burke-Ernzerhof (PBE) generalized gradient approximation (GGA) to treat the exchange–correlation energy of interacting electrons.\textsuperscript{6,7,15} A plane-wave basis set was used to expand the wave functions up to a kinetic energy cutoff value of 650 eV. A monolayer structure of C$_3$N is shown in Fig. 1. To avoid the inter-layer interaction between layers and simulate period boundary conditions, a vacuum of about 30 Å along the z direction was employed. In our study, we adopt 19 × 19 × 1 k-point in the unit cell to calculate the electronic density of states. Other calculations such as band structure and optical properties took the Gamma central k-point in the unit cell C$_3$N and 3 × 3 × 1 supercell C$_3$N are put in the Brillouin zone of the unit cell also is 9 × 9 × 1.

Monolayer C$_3$N belongs to the space group P6/mmm. The lattice parameter for it is a = 4.86 Å. The applied in-layer strain in our study is defined as $\epsilon^\% = (a – a_0)/a_0$, where $a$ is the lattice constants of the strained structure and $a_0$ is the lattice constants of strain free structure. The strain within the suitable range from −10% compressive strain to 10% tensile strain was applied in either uniaxial or biaxial direction to explore its effects on the electronic and optical properties. Because the structure of C$_3$N exhibits a high symmetry, the uniaxial strain along the $a$ lattice vector direction could be regarded as equivalent to the uniaxial strain along the $b$ lattice vector direction. So the uniaxial strain we adopted in this paper is the uniaxial strain along the direction of the lattice vector $a$. With each uniaxial or biaxial strain applied, the structure was fully relaxed.

When first-principles calculations are used to measure optical properties, the results are varied when different methods are being used. Each method has its own advantages and disadvantages.\textsuperscript{43} H–F based methods are the most efficient one among the three methods, but the spectrum higher energy peaks are missing.\textsuperscript{43} TDDFT is less efficient compared with H–F based methods, and the spectrum can be obtained in both visible and ultraviolet region.\textsuperscript{42} However, some of the low energy peaks in the spectrum region are missing.\textsuperscript{42} As for perturbation theory method, it is not as efficient as the first two methods mentioned above and requires more time and calculated resources. However, it could be more accurate in whole energy regions.\textsuperscript{44} Therefore, in calculation of the optical properties in this paper, perturbation theory method was used based on VASP code. The relevant parameters such as reflectivity $R(\omega)$, refractive index $N(\omega)$, absorption coefficient $I(\omega)$ were obtained from the results of dynamical dielectric response functions $\varepsilon(\omega)$. The computational formulas between $\varepsilon(\omega)$ and the relevant optical parameters were as follows:

\begin{align}
\varepsilon(\omega) &= \varepsilon_1(\omega) + i\varepsilon_2(\omega), \quad (1) \\
R(\omega) &= \frac{\sqrt{\varepsilon(\omega) – 1}}{\sqrt{\varepsilon(\omega) + 1}} = \frac{(n – 1)^2 + k^2}{(n + 1)^2 + k^2}, \quad (2) \\
N(\omega) &= n(\omega) + ik(\omega), \quad (3) \\
I(\omega) &= (\sqrt{2})^\omega \left[ \sqrt{\varepsilon_1(\omega)^2 + \varepsilon_2(\omega)^2} – \varepsilon_1(\omega) \right]^{1/2}. \quad (4)
\end{align}

3 Results

3.1 Strain effect on the structural properties of monolayer C$_3$N

To deeply study the uniaxial strain and biaxial strain effect on the optical properties and electronic properties of monolayer C$_3$N, the structural properties of monolayer C$_3$N must be firstly

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**Fig. 1** Top view and side view optimized atomic configuration of monolayer C$_3$N. (a1)–(a3) is the bond length between C and C atoms in different position. (b1)–(b5) is the bond length between C and N atoms in different position.
addressed. Fig. 1 exhibits the structure of monolayer C₃N. Monolayer C₃N belongs to the space group P6/mmm. The lattice parameters for it are \( a_0 = b_0 = 4.86 \, \text{Å} \). In this study, the structure of monolayer C₃N we built is composed of a number of hexagonal C rings with N atomics connecting them, which is the same as the structure in the existing experiment of monolayer C₃N.\(^{37}\) After fully relaxed the monolayer structure of C₃N, all atoms tend to be remain in one flat sheet, just like graphene. The optimized structural parameters are list in Table 1.

To confirm the stability of monolayer C₃N, we examined the phonon spectra of monolayer C₃N by using linear response method based on CASTEP package and found no imaginary phonon modes over the entire Brillouin zone (BZ) (Fig. 2), indicating the structure of monolayer C₃N is dynamically stable. This result consists well with the previous study.\(^{44}\) Further more, the optimized values of lattice constant, total energy of system (\( E_{\text{tot}} \)), bond length between C and C (\( d_{\text{C-C}} \)), bond length between C and N (\( d_{\text{C-N}} \)) and the band gap (\( E_{\text{gap}} \)) of strain free monolayer C₃N are given in Table 1. Combined with Fig. 1 and Table 1, we can see that the monolayer C₃N exhibits high geometric symmetry along the directions of \( a \) lattice vector and \( b \) lattice vector.

We next turn to discuss the in-layer strain effect on the change of structural properties (Fig. 3). Firstly, the strain energy, which defined as the difference in the energy between the strained C₃N and the strain free C₃N,\(^{45}\) of system increases with both increasing the compressive strain (from 0% to −10%) and tensile strain (from 0% to 10%). As we can see, the minimum strain energy is located at \( \varepsilon = 0\% \), that is to say, the most stable structure of monolayer C₃N is the strain free structure. Secondly, the optimized lattice constant \( a \) and \( b \) of monolayer C₃N increases linearly with altering the biaxial strain from \( \varepsilon = −10\% \) to \( \varepsilon = 10\% \). And lattice constant \( a \) is equal to \( b \) throughout the process when altering the biaxial strain from \( \varepsilon = −10\% \) to \( \varepsilon = 10\% \). However, when we applied uniaxial strain along \( a \) lattice vector, the optimized lattice constant \( a \) and \( b \) of monolayer C₃N increases nonlinearly by altering the uniaxial strain from \( \varepsilon = −10\% \) to \( \varepsilon = 10\% \). What’s more, by changing the uniaxial strain, the change of lattice constant \( a \) is much larger than that of lattice constant \( b \) which indicated that monolayer C₃N has anisotropic property when applying uniaxial strain. Thirdly, the bond length of monolayer C₃N is increasing continuously with altering strain from −10% to 10%, however, when biaxial strain is applied, all C–C bond lengths are the same and all C–N bond lengths are the same. When uniaxial strain is applied, the lengths of C–C bond and C–N bond at different positions are different, and their variations are different. As we can see, the structural property of monolayer C₃N reveals isotropy when biaxial strain is applied, and anisotropy when uniaxial strain is applied.

### 3.2 Strain effect on the electronic properties of monolayer C₃N

In terms of electronic properties, first of all, we explored the electronic properties of strain free monolayer C₃N. The band structure and density of states of strain free monolayer C₃N are calculated by PBE method. What’s more, the HSE06 method is utilized to revise the band gap (Fig. 4). We can see that monolayer C₃N exhibit semiconductivity with an indirect band gap which corresponding band gaps are 0.39 eV by using PBE method and 0.94 eV by using HSE06 method when the strain is 0%. The stable semiconductive character of C₃N in our study has also been proved in the experiment.\(^{37}\) Our results of the band gap are good agreement with the previous theoretical results.\(^{32–35}\) We compared the experimental and theoretical results of band gap as shown in Table 2. The valence band maximum (VBM) of monolayer C₃N is located at \( \Gamma \) point and the conduction band minimum (CBM) is located at \( \Gamma \) point when strain is 0% (Fig. 4(a) and (b)). According to the analysis of the PDOS of strain free monolayer C₃N, as showed in Fig. 4(c1)–(d3), the VBM and CBM are occupied by py orbital of both N and C atoms.

Furthermore, due to the carrier transport has close relationship with the properties of different frontier states, we next discuss the character of frontier states in strain free monolayer C₃N.

Fig. 5(a) and (b) display the electron partial charge density of VBM mainly derives from C and N atoms. The partial charge density of CBM mainly induced by C atoms, while a small part comes from N atom. This result consists well with the result of the analysis of PDOS (Fig. 5).

Then we consider the changes of electronic properties of monolayer C₃N by applying biaxial strain and uniaxial strain. Fig. 6 illustrates the calculated band gap of monolayer C₃N as a function of biaxial strain applied \( \varepsilon \) and uniaxial strain applied \( \varepsilon \) by using PBE and HSE06 methods, respectively. With regard to this figure, the band gap of monolayer C₃N basically keeps increasing with the either biaxial strain or uniaxial strain changes from −6% compressive strain to 10% tensile strain. The most striking distinction between the PBE method and the HSE06 method is that when the compressive strain is greater than −8%, the band gap becomes zero when the PBE method is used, while the band gap does not come to zero when the HSE06 method is used. The main reason for this difference is that the PBE method underestimates the band gap, while the HSE06 method could further revise the band gap. Based on the HSE06 calculation, monolayer C₃N could maintain indirect semiconductive characters under different biaxial and uniaxial strain from \( \varepsilon = −10\% \) to \( \varepsilon = 10\% \).

Above results reveal that monolayer C₃N exhibits semiconductivity with an moderate indirect band gap, and it can maintain this semiconductor character when biaxial or uniaxial

### Table 1 Basic optimized properties of monolayer C₃N, \( a_0 \) is the lattice constant, \( d_{\text{C-C}} \) is the bond length of C and C, \( d_{\text{C-N}} \) is the bond length of C and N

| Space group | \( a_0 = b_0 \) (Å) | \( d_{\text{C-C}} \) (Å) | \( d_{\text{C-N}} \) (Å) |
|-------------|-----------------|----------------|----------------|
| C₃N P6/mmm  | 4.86            | 1.403          | 1.403          |
|             | 4.8614 (ref. 38)| 1.4 (ref. 38)  | 1.4 (ref. 38)  |
|             | 4.862 (ref. 39) | 1.404 (ref. 39)| 1.403 (ref. 39)|
|             | 4.86 (ref. 40)  |                |                |
|             | 4.863 (ref. 41) | 1.404 (ref. 41)| 1.403 (ref. 41)|
strain applied in the range from $\varepsilon = -10\%$ to $\varepsilon = 10\%$. In addition the band gap of monolayer C$_3$N could be tuned easily via strain and the changes of electronic properties of monolayer C$_3$N by applying uniaxial strain and biaxial strain are different. All these results indicate that monolayer C$_3$N should be suitable for the applications in nanoelectronics.

Fig. 2  The phonon dispersion spectrum for monolayer C$_3$N.

Fig. 3  Basic optimized properties of C$_3$N monolayer in different strain (from $-10\%$ to $10\%$). Panel (a) displays the strain energy of C$_3$N system by applying uniaxial strain (black) and biaxial strain (red) reflectivity. In panel (b), different points represent the lattice constant of C$_3$N under different uniaxial strain respectively. In panel (c) the different point represent the bond length of C–C and C–N when uniaxial strain applied, respectively. In panel (d), different points represent the lattice constant of C$_3$N under different biaxial strain respectively. In panel (e) the different point represent the bond length of C–C and C–N when biaxial strain applied, respectively.
3.3 Strain effect on the optical properties of monolayer C$_3$N

Above calculations reveal that monolayer C$_3$N shows high stability and suitable band gap, turning it into a promising optoelectronic application. In terms of the calculations of optical properties, we also use PBE method to study its optical properties, and the HSE06 method is used to further modify the absorption edge and reflective coefficient. The primary task of optical calculation is solving the imaginary part and real part of the frequency dependent dielectric function $\varepsilon(\omega)$.

In our calculation, the frequency dependent imaginary part of the dielectric function is defined as follow:

$$
\varepsilon_2(\omega) = \frac{4\pi^2\varepsilon_0^2}{\Omega} \lim_{q \to 0} \frac{1}{q^2} \sum_{c,v,k} 2w_c \delta(\varepsilon_c - \varepsilon_v - \omega) \\
\times \langle u_{ck+c}\psi | u_{ck}\rangle \langle u_{ck+c}\psi | u_{ck}\rangle^* 
$$

(5)

In this equation, $c$ and $v$ refer to conduction and valence band states respectively, and $u_{ck}$ is the cell periodic part of the wavefunctions at the $k$-point $k$. In addition, the real part of the dielectric function is obtained by the eqn (6) as follow.

$$
\varepsilon_1(\omega) = 1 + \frac{2}{\pi} \int_0^\infty \frac{\varepsilon_2(\omega')}{\omega'^2 - \omega^2 + i\eta} d\omega' 
$$

(6)

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Table 2  Band gap of monolayer C$_3$N

| C$_3$N | Theoretical | HSE06 | Experimental |
|-------|-------------|-------|--------------|
| Method | PBE         | 0.39 (this work) | 0.94 (this work) | 2.67 (ref. 37) |
| Band gap (eV) | 0.39 (ref. 38) | 1.03 (ref. 36) | 0.39 (ref. 39) | 1.05 (ref. 38) |
|        | 0.39 (ref. 40) | 1.042 (ref. 39) | 1.09 (ref. 40) |

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Fig. 4  Calculated electronic properties of strain free monolayer C$_3$N. (a) and (b) show the band structure of strain free C$_3$N by using HSE06 method and PBE method respectively. (c1)–(c3) display the electronic density of states of strain free C$_3$N by using HSE06 method. (d1)–(d3) display the electronic density of states of strain free C$_3$N by using PBE method.

Fig. 5  The charge density for monolayer C$_3$N respectively. (a) Shows the top view of charge density for VBM of monolayer C$_3$N. (b) Shows the top view of charge density for CBM of monolayer C$_3$N.
In eqn (6), index $P$ denotes the principle value.\textsuperscript{31} By computing the dielectric function, the absorption and reflectivity spectra of monolayer C$_3$N can be obtained by using eqn (1)–(5).

Firstly, we consider the optical properties of strain free monolayer C$_3$N. We can get similar results of optical properties by using both PBE and HSE06 methods. The main differences in the results between the two methods lie in the differences of optical absorption edges, static dielectric constants, reflective coefficient and the peak value of each curve.

The results are as follows: firstly, we studied the optical absorption properties of monolayer C$_3$N by analyzing the imaginary part of dielectric function diagram and the optical absorption coefficient spectra (Fig. 7 and 8). Results obtained by PBE method indicate the optical absorption edge of monolayer C$_3$N is 0.7 eV and the first absorption peak at 2.24 eV (Fig. 7). When the HSE06 method was used, photons were absorbed by strain free monolayer C$_3$N start to absorb photons nearly in 1.5 eV, and the first absorption peak is around 3.1 eV (Fig. 8). What’s more, the absorption spectrum shows that the main absorption region of strain free monolayer C$_3$N includes basically all visible light areas (1.6–3.1 eV) by using both PBE method and HSE06 method. Secondly, we studied the optical reflectivity properties of monolayer C$_3$N by analyzing the real part of dielectric function diagram and the optical reflectivity spectra (Fig. 7 and 8). The results exhibit the static dielectric constant and static reflectivity of monolayer C$_3$N are 2.96 and 0.07 by using PBE method (Fig. 7) and 1.9 and 0.025 by using HSE06 method (Fig. 8).
Our results reveal that strain free monolayer C$_3$N display the same exciton effect along the armchair and zigzag directions which mean the optical absorption property of strain free monolayer C$_3$N are isotropic along the armchair and zigzag directions.

When in-layer strain is applied, the variations of optical properties of monolayer C$_3$N are as follows. Fig. 9(c1) and 10(c1) show the effects of biaxial strain on the optical absorption properties of monolayer C$_3$N obtained by PBE method and HSE06 method respectively. We can see that, firstly, the absorption edge almost remains unchanged when the biaxial strain alters from $\varepsilon = 3 \frac{\alpha}{C_0}$ 10% to $\varepsilon = 3 \frac{\alpha}{C_0} 10%$. Secondly, the major characteristic peaks of optical absorption vary significantly. Particularly, the first absorption peak decreases when changing the biaxial strain from $\varepsilon = 0\%$ to $\varepsilon = 10\%$ and increases when changing the biaxial strain from $\varepsilon = 0\%$ to $\varepsilon = -10\%$. The first absorption peak exhibits a red-shift from $\varepsilon = 3 \frac{\alpha}{C_0} 10\%$ and a blue-shift from $\varepsilon = 3 \frac{\alpha}{C_0} 0\%$ to $\varepsilon = 3 \frac{\alpha}{C_0} 10\%$. What’s more, when uniaxial tensile strain is applied, a new absorption peak appears in the deep ultraviolet region near 12 eV. When altering the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = 10\%$, this new peak increases and exhibits a red-shift. For armchair direction, firstly, the absorption edge almost remains unchanged when the uniaxial strain alters from $\varepsilon = 3 \frac{\alpha}{C_0} -10\%$ to $\varepsilon = 3 \frac{\alpha}{C_0} 10\%$. Secondly, the first absorption peak decreases when changing the biaxial strain from $\varepsilon = 0\%$ to $\varepsilon = \pm 10\%$. The first absorption peak exhibits a blue-shift from $\varepsilon = 3 \frac{\alpha}{C_0} 0\%$ to $\varepsilon = 3 \frac{\alpha}{C_0} -10\%$ and a red-shift from $\varepsilon = 3 \frac{\alpha}{C_0} 0\%$ to $\varepsilon = 3 \frac{\alpha}{C_0} 10\%$. What’s more, when uniaxial tensile strain is applied, a new absorption peak appears in the deep ultraviolet region near 12 eV. When altering the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = 10\%$, this new peak increases and exhibits a red-shift. For zigzag direction, firstly, the absorption edge almost remains unchanged when the biaxial strain alters from $\varepsilon = 3 \frac{\alpha}{C_0} -10\%$ to $\varepsilon = 3 \frac{\alpha}{C_0} 10\%$.}

**Fig. 8** Optical spectra of monolayer C$_3$N by using HSE06 method. 4 panels indicate the calculated values of imaginary part of dielectric function $\varepsilon_2$, real part of dielectric function $\varepsilon_1$, optical reflectivity coefficient $R$ and optical absorption coefficient $I$, respectively.
Firstly, the first absorption peak decreases when changing the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = 10\%$ and increases when changing the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = -10\%$. The first absorption peak exhibits a red-shift from $\varepsilon = 0\%$ to $\varepsilon = 10\%$. What’s more, when uniaxial tensile strain is applied, a new absorption peak appears in the deep ultraviolet region near 12 eV. The value of this peak along zigzag direction is much lower than it along armchair direction, when altering the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = 10\%$, this new peak increases and exhibits a red-shift. When altering the uniaxial strain from $\varepsilon = 0\%$ to $\varepsilon = -10\%$, this new peak decreases and exhibits a blue-shift (Fig. 9(b1) and 10(b1)). Thirdly, the variations of optical reflectivity properties of monolayer C$_3$N with changing the uniaxial strain are analyzed from the optical reflectivity coefficient spectra (Fig. 9(b2) and 10(b2)). The static reflectivity of monolayer C$_3$N increases from $\varepsilon = 0\%$ to $\varepsilon = -10\%$ and decreases from $\varepsilon = 0\%$ to $\varepsilon = 10\%$.

Above results indicates that the absorption and reflectivity properties along armchair and zigzag directions exhibit anisotropic property when we applied uniaxial strain. However, when we applied biaxial strain, the absorption and reflectivity properties along armchair and zigzag directions show isotropic property. Moreover, uniaxial tensile strain and biaxial tensile strain could cause the high absorption coefficient of monolayer C$_3$N in the deep ultraviolet region.

Combined with the results of the structural property, we suggest that, when biaxial strain is applied, the isotropic structural property induced the isotropic optical property of monolayer C$_3$N. However, when uniaxial strain is applied, the completely different response of C–C and C–N chemical bond in
different positions caused the anisotropic structural property which induced the anisotropic optical property of monolayer C$_3$N.

We have calculated the electron density distribution in the corresponding energy range of the valence electron under different strains and made a figure of it based on the result (Fig. 11). From the calculated results, we found that when uniaxial tensile strain is applied, the appearance of the new absorption peak in the deep ultraviolet region near 12 eV when uniaxial tensile strain is applied is because of the electronic transitions between N p$_z$ orbitals to conductive band.

It can be seen that the optical properties of monolayer C$_3$N are the same as those of two-dimensional materials such as black phosphene and BC$_3$, which can be effectively tuned by the applied strain. However, the optical properties of these 2D monolayer materials have their own characteristics when the applied strain changes. For example, when the strain changes from compressive strain to tensile strain, the absorption edge of BC$_3$ displays a blue shift and the static reflectivity coefficient decreases, while the absorption edge of black phosphene shows a red shift and the peak value of absorption coefficient decreases. Especially, 2D C$_3$N exhibits a unique characteristic when tensile strain is applied. It produces an obvious absorption peak in the deep ultraviolet region.

In addition, the optical anisotropy of black phosphene has been studied experimentally by Wang et al. The optical properties obtained from the Raman spectra and photoluminescence spectra in their work are in good agreement with first-principles calculations. Their work not only provides experimental guidance for the practical synthesis of 2D

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**Fig. 10** Optical spectra of monolayer C$_3$N by applying different uniaxial strain and biaxial strain obtained by HSE06 method. Panels (a1) and (b1) represent the optical absorption coefficient $I$ of monolayer C$_3$N along the armchair direction and zigzag direction when uniaxial strain applied, respectively. Panels (a2) and (b2) represent the optical reflectivity coefficient $R$ of monolayer C$_3$N along the zigzag direction when uniaxial strain applied, respectively. Panels (c1) and (c2) exhibit the variations of optical absorption coefficient $I$ and optical reflectivity coefficient $R$ of monolayer C$_3$N when biaxial strain applied, respectively.
materials and the rational application of their optical properties but also proves the correctness of theoretical research for 2D materials. Encouraged by their work, we hope that monolayer C₃N would be a promising candidate for the strain tunable optoelectronic materials in the future.

4 Conclusions

We have systematically presented a first-principles investigation of the electronic and optical properties of a new two-dimensional (2D) monolayer C₃N under different strains. The PBE method is used to calculate the electronic and optical properties, and the hybrid functional HSE06 method is used to further modify the band gap and optical absorption edge. Based on the HSE06 calculation, monolayer C₃N could maintain an indirect semiconductive character under different biaxial and uniaxial strain from $\varepsilon = -10\%$ to $\varepsilon = 10\%$. In terms of the optical property, first of all, we have found that both uniaxial tensile strain and biaxial tensile strain can lead to a high absorption coefficient of monolayer C₃N in a deep UV region. Moreover, an anisotropic optical property is presented when uniaxial strain is applied, while an isotropic optical property is shown when we applied biaxial strain. Therefore, strain engineering can be an effective approach to change the electronic and optical properties of monolayer C₃N. Based on our study, we believe that monolayer C₃N is a promising candidate in the applications of optoelectronics and nanoelectronics.

Author contributions

Qing-Yuan Chen carried out the DFT calculations and prepared the manuscript. M. Y. L., C. C. and Y. H. Contributed the discussion and suggestions. All authors read the manuscript.

Conflicts of interest

The authors declare no competing financial interests.

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References

1. H. Guo, N. Lu, L. Wang, X. Wu and X. C. Zeng, Tuning Electronic and Magnetic properties of early transition-metal dichalcogenides via Tensile strain, J. Phys. Chem. C, 2014, 118, 7241–7249.

2. K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, L. V. Grigorieva and A. A. Firsov, Electric Field Effect on Atomically Thin Carbon Films, Science, 2004, 306, 666–669.

3. N. Lu, Z. Li and J. Yang, Electronic Structure Engineering via On Plane Chemical Functionalization: A Comparison Study on Two Dimensional Polysilane and Graphene, J. Phys. Chem. C, 2009, 113, 16741–16746.

4. H. Guo, Y. Zhao, N. Lu, E. Kan, X. C. Zeng, X. Wu and J. Yang, Tunable Magnetism in a Nonmetal-Substituted ZnO Monolayer: A First-Principles Study, J. Phys. Chem. C, 2012, 116, 11336–11342.

5. J. Dai, X. Wu, J. Yang and X. C. Zeng, Unusual Metallic Microporous Boron Nitride Networks, J. Phys. Chem. Lett., 2013, 4, 3484–3488.

6. H. Liu, A. T. Neal, Z. Zhu, Z. Luo, X. Xu, D. Tománek and P. D. Ye, Phosphorene: an unexplored 2D semiconductor with a high hole mobility, ACS Nano, 2014, 8, 4033–4041.

7. L. Li, Y. Yu, G. J. Ye, Q. Ge, X. Ou, H. Wu, D. Feng, X. H. Chen and Y. Zhang, Black phosphorus field-effect transistors, Nat. Nanotechnol., 2014, 9, 372.

8. C. Si, Z. Liu, W. Duan and F. Liu, First-principles calculations on the effect of doping and biaxial tensile strain on electron-phonon coupling in graphene, Phys. Rev. Lett., 2013, 111, 196802.

9. X. Chen, Y. Liu, B.-L. Gu, W. Duan and F. Liu, Giant room-temperature spin caloritronics in spin-semiconducting graphene nanoribbons, Phys. Rev. B: Condens. Matter Mater. Phys., 2014, 90, 121403.

10. Q. Ke, C. Tang, Y. Liu, H. Liu and J. Wang, Intercalating graphene with clusters of Fe2O4 nanocrystals for electrochemical super- capacitors, Mater. Res. Express, 2014, 1, 025015.

11. Q. Ke, Y. Liu, H. Liu, Y. Zhang, Y. Hu and J. Wang, Surfactant-modified chemically reduced graphene oxide for electro-chemical supercapacitors, RSC Adv., 2014, 4, 26398–26406.

12. S. Bertolazzi, D. Krasnozhon and A. Kis, Nonvolatile memory cells based on MoS2/graphene heterostructures, ACS Nano, 2013, 7(4), 3246–3252.

13. E. Zhang, W. Wang, C. Zhang, Y. Jin, G. Zhu, Q. Sun, D. W. Zhang, P. Zhou and F. Xiu, Tunable charge-trap memory based on few-layer MoS2, ACS Nano, 2014, 9(1), 612–619.

14. C. O. H. Hugh and J. H. Pablo, Two-dimensional crystals: phosphorus joins the family, Nat. Nanotechnol., 2014, 9, 330–331.

15. A. Brown and S. Rundqvist, Refinement of the crystal structure of black phosphorus, Acta Crystallogr., 1965, 19, 684.

16. S. Zhao, W. Kang and J. Xue, The potential application of phosphorene as an anode material in Li-ion batteries, J. Mater. Chem. A, 2014, 2, 19046–19052.

17. J. Guan, Z. Zhu and D. Tománek, Phase coexistence and metal-insulator transition in few-layer phosphorene: a computational study, Phys. Rev. Lett., 2014, 113, 046804.

18. J. Mahmood, E. K. Lee, M. Jung, D. Shin, H. J. Choi, J. M. Seo, S. M. Jung, D. Kim, F. Li, M. S. Lah, et al., Two-Dimensional Polyaniline (C3N) from Carbonized Organic Single Crystals in Solid State, Proc. Natl. Acad. Sci. U. S. A., 2016, 113, 7414–7419.

19. J. D. Wood, S. A. Wells, D. Jariwala, K.-S. Chen, E. Cho, V. K. Sangwan, X. Liu, L. J. Lauhon, T. J. Marks and M. C. Hersam, Effective passivation of exfoliated black phosphorus transistors against ambient degradation, Nano Lett., 2014, 14, 6964.

20. J.-S. Kim, Y. Liu, W. Zhu, S. Kim, D. Wu, L. Tao, A. Dodabalapur, K. Lai and D. Akinwande, Toward air-stable multilayer phosphorene thin-films and transistors, Sci. Rep., 2015, 5, 89.

21. N. V. Blinova, J. Stejskal, M. Trchova, G. Ciric-Marjanovic and I. Sapurina, Polymerization of Aniline on Polyaniline Membranes, J. Phys. Chem. B, 2007, 111, 2440–2448.

22. M. Y. Chang, C. S. Wu, Y. F. Chen, B. Z. Hsieh, W. Y. Huang, K. S. Ho, T. H. Hsieh and Y. K. Han, Polymer Solar Cells Incorporating One-Dimensional Polyaniline Nanotubes, Org. Electron., 2008, 9, 1136–1139.

23. M. M. Alam, J. Wang, Y. Guo, S. P. Lee and H. R. Tseng, Electrolyte-Gated Transistors Based on Conducting Polymer Nanowire Junction Arrays, J. Phys. Chem. B, 2005, 109, 12777–12784.

24. G. Ciric-Marjanovic, Recent Advances in Polyaniline Research: Polymerization Mechanisms, Structural Aspects, Properties and Applications, Synth. Met., 2013, 177, 1–47.

25. H. J. Xiang, B. Huang, Z. Y. Li, S. H. Wei, J. L. Yang and X. G. Gong, Ordered Semiconductor Nitrogen-Graphene Alloys, Phys. Rev. X., 2012, 2, 011003.

26. P. F. Blochl, Projector augmented-wave method, Phys. Rev. B: Condens. Matter Mater. Phys., 1994, 50, 17953.

27. G. Kresse and D. Joubert, From ultraso...
31 X. Peng, A. Copple and Q. Wei, Strain-engineered direct-indirect band gap transition and its mechanism in two-dimensional phosphorene, Phys. Rev. B: Condens. Matter Mater. Phys., 2014, 90, 085402.

32 C. Zhang, Y. Jiao, T. He, S. Bottle, T. Frauenheim and A. Du, Predicting Two-Dimensional C3B/C3N van der Waals p–n Heterojunction with Strong Interlayer Electron Coupling and Enhanced Photocurrent, J. Phys. Chem. Lett., 2018, 9, 858–862.

33 Y. Qie, J. Liu, S. Wang, S. Gong and Q. Sun, C3B monolayer as an anchoring material for lithium-sulfur batteries, Carbon, 2018, 129, 38–44.

34 L. Shi, Y. Zhang, X. Xiu and H. Dong, Structural characteristics and strain behavior of two-dimensional C3N: first principles calculations, Carbon, 2018, 134, 103–111.

35 X. Zhou, W. Feng, S. Guan, B. Fu, W. Su and Y. Yao, Computational characterization of monolayer C3N: a two-dimensional nitrogen-graphene crystal, J. Mater. Res., 2017, 32, 15.

36 L. Xie, L. Yang, W. Ge, X. Wang and J. Jiang, Bandgap tuning of C3N monolayer: a first-principles study, Chem. Phys., 2019, 520, 40–46.

37 J. Mahmood, E. K. Lee, M. Jung, D. Shin, H. J. Choi, J. M. Seo, S. M. Jung, D. Kim, F. Li, M. S. Lah, N. Park, H. J. Shin, J. H. Oh and J. B. Baek, Two-dimensional polyalanine (C3N) from carbonized organic single crystals in solid state, Proc. Natl. Acad. Sci. U. S. A., 2016, 113, 7414–7419.

38 M. Makaremi, B. Mortazavi and C. V. Singh, Adsorption of Metallic, Metalloidic, and Nonmetallic Adatoms on Two-Dimensional C3N, J. Phys. Chem. C, 2017, 121, 18575–18583.

39 X. Zhou, W. Feng, S. Guan, B. Fu, W. Su and Y. Yao, Computational characterization of monolayer C3N: a two-dimensional nitrogen-graphene crystal, J. Mater. Res., 2017, 32, 2993–3001.

40 C. Zhang, Y. Jiao, T. He, S. Bottle, T. Frauenheim and A. Du, Predicting Two-Dimensional C3B/C3N van der Waals p–n Heterojunction with Strong Interlayer Electron Coupling and Enhanced Photocurrent, J. Phys. Chem. Lett., 2018, 9, 858–862.

41 X. Wang and J. Chen, Phonon-mediated superconductivity in charge doped and Li-deposited two dimensional C3N, Phys. C, 2019, 558, 12–16.

42 R. K. Shivade and B. Chakraborty, Optical absorption spectra of boron clusters Bn (n = 2–5) for application in nano scintillator – a time dependent density functional theory study, Eur. Phys. J. B, 2016, 89, 198.

43 S. Kumar, S. Sharma, V. Babar and U. Schwingenschlögl, Ultralow lattice thermal conductivity in monolayer C3N as compared to graphene, J. Mater. Chem. A, 2017, 5, 20407–20411.

44 Y. Zhang, Z.-F. Wu, P.-F. Gao, D.-Q. Fang, E.-H. Zhang and S.-L. Zhang, Strain-tunable electronic and optical properties of C3B monolayer, RSC Adv., 2018, 8, 1686–1692.

45 Z. Xie, L. Hui, J. Wang, G. A. Zhu, Z. Chen and C. Li, Electronic and optical properties of monolayer black phosphorus induced by bi-axial strain, Comput. Mater. Sci., 2018, 144, 304–314.

46 X. Wang, A. M. Jones, K. L. Seyler, V. Tran, Y. Jia, H. Zhao, H. Wang, L. Yang, X. Xu and F. Xia, Highly anisotropic and robust excitons in monolayer black phosphorus, Nat. Nanotechnol., 2015, 10(6), 517–521.

47 G. Yang, T. Ma and X. Peng, Superior mechanical flexibility and strain-engineered direct-indirect band gap transition of green phosphorene, Appl. Phys. Lett., 2018, 112, 241904.