Refractive Index, Temperature and Pressure of Elliptical Plasmonic Waveguide Resonator

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Abstract
This paper proposes the elliptical-shaped based on two-dimensional Metal-Insulator-Metal (MIM) plasmonic waveguide configuration with the sensor characteristics simulated by Finite-Element-Method (FEM). Temperature, refractive index, and pressure are evaluated in the structure by considering the transmission spectrum. As the temperature and refractive index increase, the corresponding curves shift to the right wavelengths. Simulation results show that resonant wavelength of nanocavity shifts to lower wavelength with increasing the pressure. It can be seen that the resonance curves between 1300nm to 1400nm are sharper than the other wavelengths in this structure. The sensitivity and the Figure of Merit (FOM) can be evaluated by considering the mentioned equations. The proposed structure could be applied to develop resonator applications with high sensitivity and tunable response.

Key-words: Temperature, Pressure, Plasmonic, Waveguide.

1. Introduction

Surface plasmon polaritons (SPPs) are electromagnetic waves that propagate at the interface between a metal and a dielectric [1]. Some of the promising applications of SPPs are found in gain medium, lasers, amplifiers [2], and sensors [3]. Plasmonic structures are attractive for the future of all-optical devices [4], such as Dielectric-Metal-Dielectric (DMD) [5], resonator structure [6], hybrid plasmonic waveguide [7], Metal-Insulator-Metal (MIM) [8] and etc. Among all suggested structures, optical sensors have been developed to measure a wide variety of parameters so far. Some of the applications of optical sensors are plasmonic sensors which are based on the pressure sensor [9,10],
biosensor [11], refractive index and temperature sensor [12] and etc. One of the most fascinating features of MIM waveguides is the construction of optical sensors by elliptical-shaped plasmonic waveguides [13, 14]. A major advantage of MIM waveguides is better confinement of light with a suitable propagation length for surface plasmon polaritons (SPPs) [15]. Increasing environmental refractive index induces dip position of the transmission spectrum shift towards longer wavelength [12]. Moreover, this scenario exists for temperature and dip minimum of the transmission spectrum.

In this paper, elliptical MIM plasmonic waveguide configuration is presented. Refractive index, temperature, and pressure sensing characteristics investigated in the structure.

The geometry of the configuration and theory are surveyed in Section 2. The results are offered in Section 3 in which the performance of the configuration with refractive index, temperature, and pressure are fully surveyed. Section 4 contains the conclusion part.

The proposed structure has potential advantages such as compact, low cost, and capability for multi-sensing applications.

2. Structure and Theory

The MIM plasmonic waveguide geometry is presented in Fig. 1. The blue and gray parts illustrate silver and silica, respectively. The physical parameters W and t are the width and port entrance thickness of the MIM waveguide, respectively. Also, h1 and h2 parameters are shown in Fig. 1. The specified values of parameters are shown in Table 1. In this analysis, at the wavelength 1550nm, the refractive index of SiO2 is 1.45. The transmittance in terms of wavelength is calculated by applying a commercial FEM, i.e. COMSOL multiphysics.

In the MIM plasmonic waveguide, the relative permittivity is defined by the Drude model [9, 15].

$$\varepsilon_m(\omega) = \varepsilon_\infty - \frac{\omega_p^2}{\omega^2 + i\gamma \omega}$$ (1)

where $\varepsilon_\infty = 3.7$ is the relative permittivity at infinite frequency. Also, $\omega_p = 9.17eV$ and $\gamma = 18meV$ are the frequency of the plasma oscillations and damping frequency, respectively.

| t    | h1    | h2    | W   | a    | b    |
|------|-------|-------|-----|------|------|
| 950nm| 1.64µm| 4.4µm | 10.73µm | 0.33µm | 0.6µm |
The dispersion of primary mode is defined as follows [19]:

\[
\frac{\varepsilon_p}{\varepsilon_m k} = \frac{1 - e^{k_w}}{1 + e^{k_w}}
\]  

(2)

\[
k = k_0 \sqrt{\left(\frac{\beta_{spp}}{k_0}\right)^2 - \varepsilon_i}, \quad p = k_0 \sqrt{\left(\frac{\beta_{spp}}{k_0}\right)^2 - \varepsilon_m}
\]  

(3)

\[
\beta_{spp} = n_{\text{eff}} k_0 = n_{\text{eff}} \frac{2\pi}{\lambda}
\]  

(4)

Here, \(\lambda\) is the wavelength in vacuum, \(\varepsilon_m\) and \(\varepsilon_i\) are metal and dielectric constant, respectively. \(n_{\text{eff}}\) is the effective refractive index of MIM waveguide, \(\beta_{spp}\) is the propagation constant of SPP and \(k_0 = \frac{2\pi}{\lambda}\) is the wavenumber.

By applying the temperature on the structure, the refractive index changes owing to the thermo-optic effect. The refractive index of SiO2 under temperature is [16]:

\[
n = 1.45 + T10^{-5}
\]  

(5)
where \( T \) and \( n \) are temperature and refractive index, respectively.
The refractive index of SiO\(_2\) under pressure is represented in this study as [10]:

\[
n = 1.45 - 0.00965P
\]  

(6)

where the pressure exerted in one direction is indicated by \( P \).

3. Results and Discussion

By using FEM and perfectly matched layers (PML), the transmission specifications of the structure are simulated. Based on the results shown in Figure 2a, the transmission spectrum indicates the minimum transmittance at the wavelength of 1371.5 nm is close to zero. The normalized electric field distribution at the wavelength of 1371.5 nm and 1400 nm which is shown in Fig. 2b,c clearly indicates the differences between the two introduced wavelengths. Due to elliptical configuration of the structure, the SPPs can be observed in three directions. By changing the refractive index, the transmission curve shifts. The change in displacement of the transmission curve is due to the effects of temperature and pressure.

In the next step, the influence of the refraction index sensitivity is studied. Figure 3a shows that transmission spectrum versus the wavelengths for different refractive index swept from 1.43 to 1.46. As refractive index increases, the transmission spectrum displays a shift towards longer wavelength. The increasing environmental refractive index that induces dip wavelength of the transmission spectrum is exhibited in Fig. 3b. The refractive index sensitivity can be defined as [17]:

\[
S = \frac{\Delta \lambda}{\Delta n}
\]  

(7)

where \( \Delta \lambda \) and \( \Delta n \) are the resonant wavelength variation and applied refractive index variation, respectively. The refractive index sensitivity can be obtained 950 nmRIU\(^{-1}\). Figure of merit (FoM) is another significant parameter providing an appropriate measurement which means the ratio of sensitivity for wavelength to the bandwidth of resonance can be defined as [6, 18]:

\[
\text{FOM} = \frac{S}{\text{FWHM}}
\]  

(8)
The value of 166 RIU$^{-1}$ is calculated in our simulation for FOM. In the next step, the temperature sensing specifications of the configuration are studied. With increasing temperature from 0 to 600°C, the resonant wavelength has a linear shift to a higher wavelength as shown in Fig. 4. The sensitivity for temperature is $\Delta \lambda / \Delta T$, this value can be obtained as 0.01 nm/°C.

Finally, the pressure variation of silica is evaluated by the transmission spectrum in the proposed wavelength. There is a linear relationship between the pressure of silica and the wavelength which can be seen in Fig. 5.

Figure 2. a) Transmission Spectrum, The Normalized $|E|$ Fields of the Structure b) at 1371.5 nm, c) at 1400 nm
Figure 3. a) The Transmission Spectrum of the Structure with different Refractive Index, b) The Dip Position Versus Refractive Index in the Wavelength Domain from 1340 nm to 1400 nm

Figure 4 - The Dip Position Versus Temperature in the Wavelength Domain from 1340 nm to 1400 nm
As pressure increases, the transmission spectrum exhibits will be shift towards lower wavelength. The FOM is enhanced at the beginning of the chart because of the sharp and higher transmitted signal. The pressure, sensitivity, and FOM of the first dip position of wavelengths are given in table 2. The table represents a suitable linear relation between the resonance wavelength and the pressure being used. The best FOM and sensitivity, related to 1Gpa.

The results of this study show different sensitivity values at different wavelengths. The designed structure offers a new concept for the compact and highly tunable plasmonic sensor design, such as nanosensor and nanolaser.

| Pressure(Gpa) | Sensitivity(nm/ Gpa) | FOM(Gpa⁻¹) |
|---------------|----------------------|------------|
| 1             | 1362.5               | 252.31     |
| 2             | 676.75               | 125.32     |
| 3             | 448                  | 82.96      |

4. Conclusion

In this article, the elliptical plasmonic structure with resonator characteristics was investigated that were affected by temperature, refractive index, and pressure. The proposed plasmonic sensor structure has potential applications in tunable multi-sensing and nanoscale industrial sensing. This work can play an important role in improving the performance of optical circuits.
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