A case study of energy efficient assembly sequence planning problem

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Abstract. Energy efficiency has become an important issue in manufacturing industry, since it is one of the biggest energy consumers in the world. Despite the importance of energy efficiency, it is much obvious that the research in assembly sequence that focus on environmental aspect is still lacking. In Assembly Sequence Planning (ASP), the research on problem optimization is mainly demanded for the effective computational approach to determine the best assembly sequence. This paper presents a case study from an electronic product assembly that considers the energy utilization during assembly process. In particular, the case study focuses to reduce the idle energy utilization in assembly process. The case study was optimized using newly proposed Moth-Flame Optimization (MFO) and then being compared with well-frequent used algorithms including Ant Colony Optimization (ACO), Particle Swarm Optimization (PSO), and Genetic Algorithm (GA). The result of the computational experiment test was divided into comparison of assembly layout between MFO proposed layout and existing layout. Besides, the statistical test involving Analysis of Variance (ANOVA) and post-hoc test of Fisher’s Least Significant Difference (LSD) were then conducted. The proposed MFO performed better in terms of the best minimum fitness (0.401681), average fitness (0.415308), standard deviation of fitness (0.022601), with appropriate computational time and power consumed. In meantime, the results also indicated that the case study was suitable in the development of energy efficient model for ASP.

1. Introduction
Assembly sequence planning (ASP) become one of the significant complex NP-hard combinatorial optimization problems, which brings attention in industry to reduce the total manufacturing cost by minimize the assembly time and energy [1]. One of the main challenges in product design and manufacturing was ASP. With involvement of many product components or parts, ASP problem was highly difficult to solve [2]. Since different sequences affects in different tooling arrangements, assembly sequence planning (ASP) is notified as the indivisible analysis part performed during initial phases of product and process design. Hence, the assembly cost, productivity and quality are directly affected by the different sequences [3]. From the possible different assembly sequences, ASP is needed to obtain the optimum assembly sequence [1]. To identify the best optimum assembly sequence, ASP optimization is demanded for effective computational approach due to the complexity of problem. In ASP optimization, the initial prominent step is to construct a representation method scheme to model the assembly problem. The modeling of assembly problem will directly impact the effectiveness of an assembly plan.

The ASP representation schemes are developed to fit with their optimization problem characteristics and attributes. These modeling approaches are specified into three major categories; part-based, task-
based and connector-based representation. According to the established research, the best accurate approach for ASP representation is by modelling base on the part of product [4]. This approach contributes to greater number of assembly sequence possibility which leads to harder optimization process. A simpler version model is then proposed, whereby the base part of product is described prior to development of the precedence constraint. The second modeling approach is notified as task-based which represents assembly task in the assembly process, instead of assembly part. During the task-based modeling process, the assembly direction needs for the definition of moving and fixed part. To conduct this type of modeling process, it must be minimum of two components for an assembly task. The least frequent modelling approach implemented in ASP optimization is referred as connector-based modeling. The appropriate optimization data and precedence relations are specified as to establish assembly model from connector structure before ASP. A connector probably be utilized to assemble more than one component. Since connector is the only modeled element, this approach stands high chance to minimize the assembly problem complexity.

The meta-heuristics soft computing approaches consisting of optimization algorithms show their predominance in solving ASP problems, which contradicted with the conventional techniques. Various prominent meta-heuristics optimization algorithms involving ant colony optimization algorithm (ACO), genetic algorithm (GA), and particle swarm optimization algorithm (PSO) have been applied through existing studies on ASP [5]. With the major attributes of ACO algorithms that are distributed computation, positive feedback and application of constructive greedy heuristic search, this type of algorithm is utilized to develop and optimize assembly sequences of mechanical products [6]. Due to its ability which easily operate large search spaces, flexibility in determining the constraints and derive in a fitness function [7]. By using directed stochastic search of product’s solution space of potential assembly plan, GA attempt to find optimal assembly plan [8]. As the platforms to find the best position in the search space, the social nature of interaction and communication of fish schooling, bird flocking and swarmning theory are stimulated by the PSO algorithm [9]. The principle and parameters of PSO algorithm greatly affects the premature convergence and stochastic stagnation performance, despite having positive attributes to solve ASP problems [5]. The consideration of sustainable manufacturing and ergonomic factors will the new directions, which should be emphasized in ASP research. Hence, due to energy utilization aspect is not considered in the original optimization problem, then the assembly tool, usage time and power rating consumption for the tool are randomly developed.

Apart from problem representation, the different optimization objectives are also become the focus aspect in solving ASP problem. Based on a literature survey, minimization of direction changes and tool are the highly frequent applied optimization objectives. In ASP, the assembly direction generally is considered in six significant directions ±x, ±y and ±z through the work. The assembly direction in workstation k, k = 1, 2, ..., m, are divided into two mentioned categories below: (1) Each time when the assembly changes in 180°, the assembly direction changes in 180° is documented as Dk, then Dk = Dk + 1. (2) The assembly direction changes in 90° is reported as Dk, as whenever the assembly direction changes in 90°, thus Dk = Dk + 1 [10]. Through the case for minimization of tool change in ASP optimization, some of the research works that applied this objective are [11], [12]. Besides these two frequent used optimization objectives, another ASP objective implemented are to minimize assembly operation type [13], [14] and assembly complexity [15]. A new objective has been proposed in optimize ASP problem which is to minimize assembly power consumption. The power rating (W) input will then be utilized to calculate energy utilization (EF) in the assembly process. Industrial case study is used as the scope for energy efficient in ASP.

2. Case Study Problem
In this research, the purpose of case study is to demonstrate the actual assembly problem in industry field using the same computational experiment procedure that have been applied previously into assembly test problems. The data of case study is taken from an electronics manufacturing factory. The data collection was made during regular working hours. During the data collection process, the raw data of case study assembly was taken from an assembly line. There were three repetitions of data performed towards the product assembly. For the optimization purpose, the size of population for each algorithm was set to 20. In each run, the maximum iteration was specified as 300.
The case study problem consists of 23 assembly parts, which are marked in numbering sequence as shown in Figure 1. The assembly directions are along the X and Y axes, for every part involved. Suppose that the assembly tool and time to assemble the base part P1 are tool (T1, T3, T2, and T6), while time (39s, 73s, 64s, and 58s) respectively. Engineering information involving the assembly parts, assembly directions, assembly time usage, and assembly power are documented in Table 1. For assembly time, the running time during assembly process is recorded as 490 seconds.

The suitable tools and connections for assembling each part in this case study are also shown in Table 1 and other assembly process constraints being excluded. Besides, the ASP information including design variables, constraint and optimization parameters can be visualized through precedence graph and data matrix.

Table 1. Assembly data for case study assembly problem.

| Part | Direction | Tool  | Time (s) | Power (W) |
|------|-----------|-------|----------|-----------|
| P1   | -z        | T1    | 39       | 120       |
| P2   | -z        | T1    | 31       | 120       |
| P3   | -z        | T2    | 48       | 380       |
| P4   | +y        | T2    | 89       | 380       |
| P5   | +y        | T3    | 27       | 420       |
| P6   | -z        | T3    | 48       | 420       |
| P7   | -z        | T3    | 73       | 420       |
| P8   | -x        | T2    | 21       | 380       |
| P9   | +y        | T2    | 64       | 380       |
| P10  | -y        | T4    | 12       | 100       |
| P11  | -z        | T4    | 15       | 100       |
| P12  | -y        | T5    | 65       | 350       |
| P13  | -y        | T6    | 58       | 240       |
| P14  | -y        | T7, T8| 60       | 1570      |
| P15  | +x        | T7, T8| 45       | 1570      |
| P16  | +x        | T9    | 32       | 0         |
| P17  | +y        | T10   | 27       | 0         |
| P18  | -z        | T11   | 70       | 2800      |
| P19  | -z        | T12   | 22       | 70        |
| P20  | -x        | T1, T13| 44 | 120       |
| P21  | -x        | T14   | 19       | 750       |
| P22  | -z        | T14   | 20       | 750       |
| P23  | -z        | -      | 34       | -         |
3. Moth-Flame Optimization (MFO) Algorithm

Moth-flame optimization (MFO) algorithm is one of the recent generated population-based developed algorithms firstly introduced by Mirjalili in 2015 [16]. MFO is referred as a novel nature-inspired method that based on transverse orientation of moths in space from navigating mechanism of moths [17]. With respect to the Moon, transverse orientation acquires efficient mechanism of traveling by utilizes constant angle which moves in straight line and fly spirally around the lights which converges, despite the availability of artificial light [18]. Moth is regarded as the candidate solution and variables are the position of moth in space [19]. Both of the solution differs in their treatment method and updating in every iteration [20].

During searching the search space, flames had been considered as flags that dropped by moths. Therefore, flames are observed as the best position gained so far. Using this method, a moth tends to not lose its best solution. To prevent local optimum stagnation, a designated flame is provided to every moth. The establishment of MFO flowchart brings more understanding towards the detailed computational process and mechanism of the algorithm [21]. It has been concerned that MFO algorithm is also part of the optimization, which involve searching the optimal values of control variables in minimizing the objective function. With converting their position vectors, the moths able to fly hyper dimensional space [17].
4. Result and Discussion

In the case study, this section is categorized into two prominent main parts that including comparison of assembly layout on MFO proposed layout with the existing layout and statistical test of case study problem. The purpose of comparison is to specify the improvement or modification made between these layouts. Meanwhile, the statistical test is performed to analyze the optimization results obtained using specific analysis testing and method. For computational experiment, the optimization is repeated 20 times to reduce the pseudo-random effect. The population size is 20, while the maximum iteration is set to 300.

Table 2 shows the optimization results for the case study on energy efficiency of ASP problem. The result is demonstrated in significant categories consisting of minimum fitness, maximum fitness, average fitness, standard deviation of fitness, and average CPU time. The best result for each problem is in bold italics. In this case study, all algorithms able to achieve minimum fitness. MFO algorithm obtained the best minimum fitness, maximum fitness and average fitness for all runs, which every moth search around the flame and update it to find a better solution. Hence, a moth keeps the best solution using this mechanism [19]. Besides, MFO algorithms also acquire the good standard deviation of fitness as compared to other algorithms. With respect to different locations in the search space, the update position of moths could potentially reduce the exploitation of best significant solutions [22]. Since the running time of optimization for each algorithm are different, the best average CPU time was belonged to MFO algorithm, followed by GA, PSO and ACO algorithms. Given the high convergence accuracy and global optimization ability, these positive attributes did contribute for MFO to achieve the best average CPU time. It was probably impossible to avoid the interruption during the optimization process as to get the accurate CPU time.

Figure 2. Flowchart of the MFO algorithm
Table 2. Computational Experiment of Case Study.

| Indicator                       | ACO   | GA     | PSO    | MFO   |
|---------------------------------|-------|--------|--------|-------|
| Minimum fitness                 | 0.404693 | 0.492716 | 0.491929 | **0.401681** |
| Maximum fitness                 | 0.476879 | 0.591107 | 0.624055 | **0.453277** |
| Average fitness                 | 0.43472   | 0.542075 | 0.562882 | **0.415308** |
| Standard deviation of fitness   | 0.024009 | 0.024597 | 0.032096 | **0.022601** |
| Average CPU time (s)            | 174.5356 | 62.25228 | 85.92661 | **58.87223** |

4.1. Comparison of Assembly Layout on MFO Proposed Layout with Existing Layout

Table 3 presents the best solution identified for case study problem on each algorithm involved. The best solution of MFO algorithm is shown in bold italic. For better explanation, the performance of MFO proposed layout was compared to existing layout of assembly objective functions as shown in Table 4. All algorithms came out with the same objective values, although there was a difference in the assembly layout. The layout of ACO was chosen since this algorithm been specified as the second best optimization algorithm after MFO. The assembly direction change is counted when the next part is assembled in different direction with the current direction. In addition, the assembly tool direction is also counted in the similar way. For the part that needs more than one tools in each algorithm, the tool changes is counted for every tool involved. There are two tools changes can be identified, for examples from P13 to P14 in the proposed MFO algorithm. For MFO layout, the number of direction change is 11, while the tool change is 19.

Table 3. Best Solution for Case Study Problem.

| Algorithm | Direction Change, DC | Tool Change, TC | Idle Energy Utilization, EI (W.h) | Assembly Sequence |
|-----------|----------------------|-----------------|-----------------------------------|-------------------|
| ACO       | 13                   | 22              | 106.5381                          | 20 1 2 3 4 5 6 7 11 8 9 10 12 13 |
|           |                      |                 |                                   | 14 15 16 19 17 21 22 23 18 |
| GA        | 17                   | 22              | 147.8816                          | 20 1 2 6 11 3 4 5 7 9 10 8 12 13 |
|           |                      |                 |                                   | 15 14 17 16 19 21 22 23 18 |
| PSO       | 19                   | 23              | 120.6245                          | 20 1 4 5 8 2 3 6 7 11 9 10 12 13 |
|           |                      |                 |                                   | 14 15 16 19 17 21 22 23 |
| **MFO**   | **11**               | **19**          | **111.6245**                      | **20 1 2 3 4 5 6 7 9 8 10 11 12 13** |
|           |                      |                 |                                   | **14 15 16 19 17 18 21 22 23** |

Table 4. Comparison of Assembly Layout.

| Objective Functions | Assembly Layout |
|---------------------|-----------------|
|                     | Existing Layout | MFO Proposed Layout |
| Number of Direction Change | 13              | 11 |
| Number of Tool Change      | 22              | 19 |
| Idle Energy Utilization     | 106.5381 W.h   | 111.6245 W.h   |
4.2. Comparison of Assembly Layout on MFO Proposed Layout with Existing Layout

The overall changes for both assembly indicators are summed up as 30. On the other hand, the number of direction change is 13 and the tool change is 22 in existing layout, leads to total changes of 35. Meanwhile, the existing layout obtain lower idle energy utilization that is better than the proposed layout. Comparison of the layout between the algorithms, the proposed layout had better assembly layout than ACO algorithm which represents the existing layout. For this case study problem, the optimization result indicates that MFO managed to acquire the best minimum fitness, maximum fitness, average fitness, standard deviation of fitness, and average CPU time. Since there were positive responses occurred, the assembly usage time and power consumption able to be minimized. Therefore, this minimization helps to increase the production output yet brings more profit. Instead of secured best fitness values, the optimization objectives did not necessarily guarantee to have the best value in all indicators. Instead, MFO had the minimum direction and tool changes, however not the best on energy utilization. Possibly, this is due to the normalizing effect and power usage consumed. A small change in direction and tool changes do brings larger consequences on the fitness, since the range of energy utilization was greater than these two objective functions.

4.3. Statistical Test of Case Study

From the optimization results obtained, the statistical test involving analysis of variance (ANOVA) and post-hoc testing must be performed for further validation between each algorithm in the case study. Table 5 presents the one-way ANOVA of single factor result for case study. This result is specified into two sources of variation consisting of between groups and within groups, which also include the sum of degrees (SS), degrees of freedom (df), mean square (MS), F (distribution), P-value, and F critical. Among the two sources of variation in one-way ANOVA, the variance within groups obtained the best sum of squares and mean squares through the analysis process. When the sum of squares is lower, the mean square subsequently became lower.

| Case Study Problem | Source of Variation | Sum of Squares (SS) | Degrees of Freedom (df) | Mean Square (MS) | F | P-value | F critical |
|--------------------|---------------------|---------------------|-------------------------|-----------------|---|---------|------------|
| Between groups     | 0.22998             | 3                   | 0.0767                  | 85.028          | 3.2E-24 | 2.7249  |
| Within groups      | 0.06852             | 76                  | 0.0009                  |                 |     |         |            |

However, the degrees of freedom for within groups variance in case study was exceptionally higher, due to total number of observations contained in all data cells. Despite minus the degrees of freedom lost during the analysis because the cell means are set, it is remaining higher. The F ratio value computed in this case study was higher than F critical value, at significant level (0.05). Since the F ratio is much larger than critical value, the null hypothesis of equal population means can be rejected. Therefore, it can be concluded that there is statistically significant difference among the population means.

Table 6 indicates indicates the post-hoc fisher’s least significant difference (LSD) analysis result for case study. Larger F ratio brings smaller P-value. Given that the P-value was less than significant level α (P ≤ 0.05), the null hypothesis H1 needs to be rejected. Hence, the statistically significant difference does exist. Since there are differences in means, the post-hoc analysis testing must be performed. The smallest significant value between the means calculated using LSD method was 0.018911, which enable direct comparisons between the means been made.

On the other hand, Table 7 presents the mean and absolute mean difference values for case study problem which derived from analysis of LSD. As the mean represent average value of each algorithm, the difference between absolute mean value were compared to LSD value. The absolute means are considered significantly different, if the difference is larger than LSD by using proposed MFO algorithm as the benchmark algorithm. However, the differences in each algorithm was found to be lower than the LSD value. Therefore, the absolute means were considered not significantly different at P ≤ 0.05. This
condition proves that LSD makes no adjustment or modification, for the fact that multiple comparisons are being conducted.

**Table 6.** Post-Hoc Fisher’s Least Significant Difference (LSD) Analysis Result for Case Study.

| Case Study Problem | Significant level, $\alpha$ | Degrees of Freedom, $df$ | Mean Square (within), $MSW$ | t-critical | $1/n_1$ | LSD |
|--------------------|----------------------------|--------------------------|-----------------------------|------------|----------|-----|
|                    | 0.05                       | 76                       | 0.000902                    | 1.99167    | 0.1      | 0.018911 |

**Table 7.** Mean and Absolute Mean Difference of LSD Analysis Result for Case Study.

| Case Study Problem | Mean | Absolute Mean Difference |
|--------------------|------|--------------------------|
|                    | MFO  | ACO          | GA         | PSO          | ACO | GA | PSO |
|                    | 1.03386 | 1.03703 | 1.02469 | 1.01553    | 0.00317 | 0.00917 | 0.01833 |

5. Conclusion

This paper modeled the case study of energy efficiency for assembly sequence planning (ASP) problem, along with number of direction changes and tool changes. The comparison of assembly layout on MFO proposed layout with existing layout was made, as to show the differences occurred in terms of objective functions used. The calculation of energy utilization using MFO algorithm was performed in this case study. In this case study, the energy utilization ($EI$) was considered during idle mode for assembly process. A newly proposed Moth-Flame Optimization (MFO) algorithm been used, which then compared with frequently applied algorithms in the optimization for ASP. An industrial case study was implemented for computational experiment. According to the optimization results, MFO algorithm managed to achieve the best minimum fitness, maximum fitness and average fitness. Besides, the computational time for MFO was also acceptable. Furthermore, MFO obtained the good standard deviation of fitness compared to other algorithms. From this paper, the finding also summarized that energy efficient can be implemented for optimization of ASP since it is still lack in the research. The proposed MFO had huge potential to be further discovered in optimized different ASP problem.

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