System-size dependence of transverse momentum correlations at $\sqrt{s_{NN}} = 62.4$ and 200 GeV at the BNL Relativistic Heavy Ion Collider

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\[ \sqrt{s_{NN}} = 62.4 \text{ and } 200 \text{ GeV} \]

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We present a study of the average transverse momentum ($p_t$) fluctuations and $p_t$ correlations for charged particles produced in Cu + Cu collisions at midrapidity for $\sqrt{s_{NN}} = 62.4$ and 200 GeV. These results are compared with those published for Au + Au collisions at the same energies, to explore the system size dependence. In addition to the collision energy and system size dependence, the $p_t$ correlation results have been studied as functions of the collision centralities, the ranges in $p_t$, the pseudorapidity $\eta$, and the azimuthal angle $\phi$. The square root of the measured $p_t$ correlations when scaled by mean $p_t$ is found to be independent of both colliding
I. INTRODUCTION

The study of event-by-event fluctuations and correlations is an important tool to understand thermalization and phase transitions in heavy-ion collisions [1–6]. Non-monotonic change in transverse momentum ($p_t$) correlations (the inversion of the mean transverse momentum fluctuations in various pseudorapidity and azimuthal angle difference regions of the produced particles) indicate that the basic correlation mechanism could be dominated by the process of parton fragmentation [7]. Thus fluctuation measurements are proposed to be an important tool in understanding nucleus-nucleus collisions [1,5,6,8–12]. In addition, under the assumption that thermodynamics is applicable to heavy-ion collisions, fluctuations in various observables could be related to thermodynamic properties of the matter formed. For example, the event-by-event ($p_t$) could be related to temperature fluctuations [13–17].

The study of event-by-event fluctuations of various quantities such as eventwise mean transverse momentum ($\langle p_t \rangle$), charged track multiplicity, and conserved quantities such as net-baryon and/or net-charge number are considered to be some of the main probes in the search for the critical point in the QCD phase diagram [17–26]. One expects enhanced fluctuations in the above observables when the system passes through the vicinity of the critical point. Recent results from CERN Super Proton Synchrotron (SPS) experiments show that the energy dependence of transverse momentum fluctuations does not show the increase expected for freeze-out near the critical point of QCD [27]. However, when these fluctuations are studied as a function of the system size (colliding C + C, Si + Si, Pb + Pb), enhanced fluctuations are observed in smaller colliding systems [28]. The results from the RHIC beam energy scan (BES) [29] data for the above observables will provide further insights.

The results presented here are from Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV using the solenoidal tracker At RHIC (STAR) and are compared with the published results from Au + Au collisions at the same energies [30]. This paper describes a systematic study of the system size dependence of the transverse momentum correlations observed at RHIC. The paper is organized as follows. The STAR detector, the data set, and the centrality selection used in the analysis are discussed in Sec. II. In Sec. III, we discuss ($p_t$) fluctuations extracted from the ($p_t$) distributions, which are compared with mixed events and gamma distributions. Dynamical fluctuations are extracted and presented for Au + Au and Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. The ($p_t$) correlations and the dynamical correlations when scaled by ($N_{\text{part}}$) and ($p_t$) are discussed in Sec. IV, to understand the centrality and energy dependence. Experimental data is also compared to various model calculations. Finally, a detailed study of $\eta$, $\phi$, and $p_t$ dependence of the correlations is presented. The systematic errors associated with the analysis are discussed in Sec. V. We conclude with a summary in Sec. VI.

II. EXPERIMENT AND DATA ANALYSIS

The Cu + Cu data were taken using the STAR detector with a minimum bias trigger. For the data taken at $\sqrt{s_{NN}} = 200$ GeV this was done by requiring a coincidence from the two zero-degree calorimeters (ZDCs). For the $\sqrt{s_{NN}} = 62.4$ GeV data, the ZDC is less efficient, so a beam beam counter (BBC) coincidence was also required. More details about the trigger detectors can be obtained from Ref. [31].

The main detector used in this analysis is the time projection chamber (TPC) [32], which is the primary tracking device in STAR. The TPC is 4.2 m long and 4 m in diameter and its acceptance spans about ±1.0 units of pseudorapidity and full azimuthal coverage. The sensitive volume of the TPC contains P10 gas (10% methane, 90% argon) regulated at 2 mbar above atmospheric pressure. The TPC data are used to determine particle trajectories, momenta, and particle type through ionization energy loss ($dE/dx$) [33].

The primary vertex of events used in this analysis is required to be within ±30 cm of the geometric center of the TPC along the beam axis. This selection process provides about 7.5 × 10$^6$ and 15 × 10$^6$ minimum bias events for Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV, respectively.

The collision centralities are represented by the fractions of events in the minimum bias inelastic cross section distribution in a collision. In data, the collision centrality is determined by using the uncorrected charged track multiplicity ($N_{\text{ch}}^{\text{TPC}}$), measured in the TPC within $|\eta| < 0.5$. The various centrality bins are calculated as a fraction of this multiplicity distribution starting at the highest multiplicities. The centrality classes for Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV are 0%–10% (most central), 10%–20%, 20%–30%, 30%–40%, 40%–50%, and 50%–60% (most peripheral). Each centrality bin is associated with an average number of participating nucleons ($\langle N_{\text{part}} \rangle$) obtained using Glauber Monte Carlo simulations [34] employing the Woods-Saxon distribution for the nucleons inside the Cu nucleus. The systematic uncertainties include those determined by varying the Woods-Saxon parameters, those associated with the nucleon-nucleon cross sections, those related to the functional representation of the multiplicity distribution, and those associated with the determination of the total Cu + Cu cross section. Table I lists the $N_{\text{ch}}^{\text{TPC}}$ and $\langle N_{\text{part}} \rangle$ values for each centrality in Cu + Cu collisions.
TABLE I. The $N_{TPC}^{ch}$ values and average number of participating nucleons ($\langle N_{part} \rangle$) for various collision centralities in Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV.

| % cross section | Cu + Cu 62.4 GeV | Cu + Cu 200 GeV |
|-----------------|------------------|-----------------|
| $N_{TPC}^{ch}$  | $\langle N_{part} \rangle$ | $N_{TPC}^{ch}$ | $\langle N_{part} \rangle$ |
| 0–10            | $\geq 101$       | $\geq 139$     | 99.0$^{+1.5}_{-1.2}$ |
| 10–20           | 71–100           | 98–138         | 74.6$^{+1.3}_{-1.0}$ |
| 20–30           | 49–70            | 67–97          | 53.7$^{+0.7}_{-0.5}$ |
| 30–40           | 33–48            | 46–66          | 37.8$^{+0.7}_{-0.5}$ |
| 40–50           | 22–32            | 30–45          | 26.2$^{+0.5}_{-0.4}$ |
| 50–60           | 14–21            | 19–29          | 17.2$^{+0.4}_{-0.2}$ |

at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. Corresponding values for Au + Au collisions can be found in Ref. [34].

In order to have uniform detector performance, a pseudorapidity cut of $|\eta| < 1.0$ is applied to tracks. To avoid the admixture of tracks from a secondary vertex, a requirement is placed on the distance of closest approach (DCA) between each track and the event vertex. The charged particle tracks are required to have originated within 1 cm of the measured event vertex. The multiple counting of split tracks (more than one track reconstructed from the original single track) is avoided by applying a condition on the number of track fit points ($N_{Fit}$) used in the reconstruction of the track. Each included track is required to have a minimum number of 21 TPC points along the track. The transverse momentum range selected for the analysis is 0.15–2.0 GeV/c.

The errors shown in the figures have the statistical and systematic errors added in quadrature unless otherwise stated. The statistical errors are small and are within symbol sizes. The final systematic errors are obtained as quadrature sums of systematic errors from different sources as discussed in Sec. V.

III. $\langle p_{T} \rangle$ FLUCTUATIONS

The $p_{T}$ fluctuations in high-energy collisions can be measured using the distribution of the eventwise mean transverse momentum defined as

$$\langle p_{T} \rangle = \frac{1}{N} \sum_{i=1}^{N} p_{T,i},$$

where $N$ is the multiplicity of accepted tracks from the primary vertex in a given event and $p_{T,i}$ is the transverse momentum of the $i$th track. The mean-$p_{T}$ distribution is compared to the corresponding distribution obtained for mixed events [30]. Mixed events are constructed by randomly selecting one track from an event chosen from the events in the same centrality and same event vertex bin. The mixed events are created with the same multiplicity distribution as that of the real events.

Figure 1 shows the event-by-event mean-$p_{T}$ distributions for 0%–10% Cu + Cu collisions at (a) $\sqrt{s_{NN}} = 200$ and (b) 62.4 GeV. The solid symbols represent the $\langle p_{T} \rangle$ distributions for data; the open symbols represent $\langle p_{T} \rangle$ distributions for mixed events. The distributions are similar for other centralities. The mixed events provide a reference measure of statistical fluctuations in the data. Any fluctuations observed in data beyond these statistical fluctuations are referred to as nonstatistical or dynamical fluctuations in this paper. For both data and mixed events, while going from central to peripheral collisions, the mean ($\mu$) of the distributions decreases whereas the standard deviation ($\sigma$) increases. Moreover, it is seen that the $\langle p_{T} \rangle$ distributions for data are wider than those for mixed events, suggesting the presence of nonstatistical fluctuations in Cu + Cu data for both 62.4 and 200 GeV collisions.

The curves in Fig. 1 represent the gamma ($\Gamma$) distributions for data (solid lines) and mixed events (dotted lines). The $\Gamma$ distribution [4,35] is given by

$$f(x) = \frac{x^{\alpha-1}e^{-x/\beta}}{\Gamma(\alpha)\beta^{\alpha}},$$

where $x$ represents the $\langle p_{T} \rangle$; $\alpha = \mu^{2}/\sigma^{2}$ and $\beta = \sigma^{2}/\mu$.

Tannenbaum [35] argues that the $\Gamma$ distribution is one of the standard representations of the inclusive single particle $p_{T}$ distribution. Tannenbaum [35] also suggests that the quantity $\alpha/\langle N_{ch} \rangle$, should be $\sim 2$, and the quantity $\beta \times \langle N_{ch} \rangle$ representing the inverse slope parameter may be referred to as the temperature of the system. Here $\langle N_{ch} \rangle$ is the average charged particle multiplicity in a given centrality bin. It is found that $\alpha/\langle N_{ch} \rangle$ for Cu + Cu 0%–10% central collisions is 2.04 at 200 GeV, and is 2.18 at 62.4 GeV. The respective $\beta \times \langle N_{ch} \rangle$ values are 0.284 GeV/c and 0.256 GeV/c. The $\alpha/\langle N_{ch} \rangle$ and $\beta \times \langle N_{ch} \rangle$ for 0%–5% central Au + Au collisions at 200 GeV were found to be 1.93 and 0.299 GeV/c [30]. Table II lists gamma-distribution parameters for event-by-event $\langle p_{T} \rangle$ distributions for data and mixed events in central (0%–10%) Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV.
TABLE II. Gamma distribution parameters for event-by-event $\langle p_t \rangle$ distributions for data and mixed events in central (0%-10%) Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV.

| Collision type (AA)          | $\alpha$ | $\beta$ | $\mu$  | $\sigma$ |
|-----------------------------|----------|---------|--------|----------|
| Cu 200 (data)               | 476      | 1.22    | 0.5805 | 0.02660  |
| Cu 200 (mixed)              | 634      | 0.92    | 0.5807 | 0.02310  |
| Cu 62.4 (data)              | 358      | 1.56    | 0.5603 | 0.02960  |
| Cu 62.4 (mixed)             | 457      | 1.23    | 0.5602 | 0.02621  |

The values for Au + Au collisions can be found in Ref. [30]. For Cu + Cu collisions at 200 GeV, $\alpha/(N_{ch})$ varies from 2.04 to 2.11 from central to peripheral collisions. However, for Cu + Cu at 62.4 GeV, $\alpha/(N_{ch})$ varies from 2.18 to 2.27 from central to peripheral collisions. The errors on values of $\alpha$ and $\beta$ are of the order of 13%–18% and 9%–12%, respectively, for Cu + Cu collisions.

The nonstatistical or dynamical fluctuations in mean $p_t$ are quantified using a variable $\sigma_{dyn}$ [36,37] defined as

$$\sigma_{dyn} = \sqrt{\frac{\sigma_{data}^2}{\mu_{data}^2} - \frac{\sigma_{mix}^2}{\mu_{mix}^2}},$$

where $\mu_{data}$ and $\mu_{mix}$ are the means of the event-by-event ($p_t$) distributions for data and mixed events, respectively. Similarly, $\sigma_{data}$ and $\sigma_{mix}$ are respectively the standard deviations of ($p_t$) distributions for data and mixed events. Figure 2 shows the dynamical fluctuations ($\sigma_{dyn}$) in mean $p_t$ plotted as a function of $\langle N_{part} \rangle$. The results are shown for Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV, and are compared with the results from Au + Au collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. The dynamical ($p_t$) fluctuations are similar in Au + Au and Cu + Cu collisions at similar values of $\langle N_{part} \rangle$. The fluctuations decrease as $\langle N_{part} \rangle$ increases. The dynamical fluctuations are also independent of the collision energy and are found to vary from ~2% to ~5% for $\langle N_{part} \rangle$ less than ~120. For $\langle N_{part} \rangle$ greater than ~150, the dynamical fluctuations are smaller and vary from 1% to 2.5%.

IV. $p_t$ Correlations

Nonstatistical or dynamical fluctuations can also be analyzed by using two-particle transverse momentum correlations [30]. The two-particle $p_t$ correlations are studied using the following equation [30]:

$$\langle \Delta p_{t,i} \Delta p_{t,j} \rangle = \frac{1}{N_{event}} \sum_{k=1}^{N_{event}} C_k,$$

where $C_k$ is the two-particle transverse momentum covariance for the $k$th event,

$$C_k = \sum_{i=1}^{N_k} \sum_{j=1, i \neq j}^{N_k} (p_{t,i} - \langle p_{t,i} \rangle)(p_{t,j} - \langle p_{t,j} \rangle),$$

where $p_{t,i}$ is the transverse momentum of the $i$th track in the $k$th event, $N_k$ is the number of tracks in the $k$th event, and $N_{event}$ is the number of events. The overall event average transverse momentum ($\langle p_{t,i} \rangle$) is given by

$$\langle p_{t,i} \rangle = \left( \sum_{k=1}^{N_{event}} \langle p_{t,i} \rangle_k \right) / N_{event}.$$

where $\langle p_{t,i} \rangle_k$ is the average transverse momentum in the $k$th event. It may be noted that, for mixed events, there will be no dynamical fluctuations and the $p_t$ correlations will be zero. Equation (4) is used to obtain the $p_t$ correlations in Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. These results are compared with the published results from Au + Au collisions at similar energies [30] to investigate the system-size and collision energy dependence of the $p_t$ correlations in heavy-ion collisions at RHIC.

The $p_t$ correlation values may be influenced by the dependence of the correlations on the size of the centrality bin due to variation of $\langle p_{t,i} \rangle$ with centrality. This dependence is removed by calculating $\langle p_{t,i} \rangle$ as a function of $\langle N_{ch} \rangle$, which is the multiplicity of charged tracks used to define the centrality. This multiplicity dependence of $\langle p_{t,i} \rangle$ is fitted with a suitable polynomial in $\langle N_{ch} \rangle$ and used in Eq. (5) for $\langle p_{t,i} \rangle$. All results presented in this paper have been corrected for this effect.

Figure 3(a) shows the $p_t$ correlations plotted as a function of $\langle N_{part} \rangle$ for Cu + Cu and Au + Au collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. The $p_t$ correlations decrease with increasing $\langle N_{part} \rangle$ for Au + Au and Cu + Cu at both energies. The decrease in correlations with increasing participating nucleons could suggest that correlations are dominated by pairs of particles that originate from the same nucleon-nucleon collision, and they get diluted when the number of participating nucleons increases [30].

A. Scaled $p_t$ correlations

The decrease in $p_t$ correlations with increasing $\langle N_{part} \rangle$ seen in Fig. 3(a) may be related to a system volume dependence characterized by $\langle N_{part} \rangle$. This volume dependence is removed by multiplying the $p_t$ correlations by $\langle N_{part} \rangle^2$ as shown in Fig. 3(b). The results are shown for Cu + Cu and Au + Au collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. It is observed that this measure of $p_t$ correlations increases quickly with increasing $\langle N_{part} \rangle$ for both Cu + Cu and Au + Au collisions.
The correlation measure $\langle p_{t,i} \Delta p_{t,j} \rangle$ may change due to changes in $\langle p_{t} \rangle$ with incident energy and/or collision centrality. To address these changes, the square roots of the measured correlations are scaled by $\langle p_{t} \rangle$. Figure 3(c) shows the corresponding quantity $\sqrt{\langle \Delta p_{t,i} \Delta p_{t,j} \rangle}/\langle p_{t} \rangle$ plotted as a function of collision centrality for Cu + Cu and Au + Au collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV. It is observed that the correlation scaled by $\langle p_{t} \rangle$ is independent of collision system size and energy, but decreases with increasing $\langle N_{\text{part}} \rangle$. The combined effect of multiplying $p_{t}$ correlations by $\langle N_{\text{part}} \rangle/2$ and scaling with $\langle p_{t} \rangle$ is shown in Fig. 3(d). It seems that this quantity $\sqrt{\langle N_{\text{part}} \rangle/2 \langle \Delta p_{t,i} \Delta p_{t,j} \rangle}/\langle p_{t} \rangle$ increases with $\langle N_{\text{part}} \rangle$ and shows saturation for central Au + Au collisions, but is independent of collision system and energy.

### B. Model comparisons

It is interesting to compare the above results with theoretical model calculations to understand the physical mechanism behind these measurements. The comparison is made with some widely used models in heavy-ion collisions such as ultrarelativistic quantum molecular dynamics (URQMD) [39], a multiphase transport model (AMPT) (default and string-melting) [40], and the heavy-ion jet interaction generator (HIJING) (with jet quenching switched off and on) [41]. The model results are obtained using URQMD version 2.3, AMPT version 1.11 for default, and version 2.11 for AMPT string melting.

HIJING is a perturbative QCD-inspired model that produces multiple minijet partons; these later get transformed into string configurations and then fragment to hadrons. The fragmentation is based on the Lund jet fragmentation model [42]. A parametrized parton-distribution function inside a nucleus is used to take into account parton shadowing.

AMPT uses the same initial conditions as in HIJING. However, the minijet partons are made to undergo scattering before they are allowed to fragment into hadrons. The string-melting (SM) version of the AMPT model (labeled here as AMPT melting) is based on the idea that, for energy densities beyond a critical value of 1 GeV/fm$^3$, the hadronic system should be deconfined. Strings are then decomposed into their partonic components. This is done by converting the mesons to a quark-antiquark pair, baryons to three quarks, and so on. The string fragmentation is based on the Lund jet fragmentation model [42]. A parametrized parton distribution function inside a nucleus is used to take into account parton shadowing.

The transport-based URQMD model calculations are observed to have a better quantitative agreement with the measurements compared to models which incorporate only jetlike correlations as in HIJING. HIJING gives similar dependence on $\langle N_{\text{part}} \rangle$ but underpredicts the magnitude. Inclusion of the jet-quenching effect in HIJING leads to a smaller value of the correlations in central collisions. AMPT model calculation incorporating coalescence as a mechanism of particle production also compares well with data for central collisions. However, the default version of this model which incorporates additional initial and final state scattering relative to HIJING yields smaller values of correlations.
C. $\eta$ and $\phi$ dependence

The $\eta$ and $\phi$ dependences of $p_t$ correlations are also studied. Figure 5 shows the $p_t$ correlations plotted as a function of increasing rapidity acceptance for Cu+Cu collisions at (a) $\sqrt{s_{NN}} = 200$ and (b) 62.4 GeV. The data points for centralities $0\%$–$10\%$, $20\%$–$30\%$, and $40\%$–$50\%$ are shifted by 0.01 in $\Delta \eta / 2$ for clarity. The correlations are almost independent of the $\Delta \eta$ window for the most central collisions. For peripheral collisions, the correlations show a slight rapidity dependence with maximum value for $-0.25 < \eta < 0.25$.

Figure 6 shows the $p_t$ correlations for varying azimuthal angle windows for Cu + Cu collisions at (a) $\sqrt{s_{NN}} = 200$ and (b) 62.4 GeV. The data points for $\Delta \phi$ windows $30^\circ$ and $90^\circ$ are shifted by 0.5 units in $\langle N_{\text{part}} \rangle$ for clarity. The $p_t$ correlations are maximum for $\Delta \phi = 15^\circ$ (among the cases studied) and decrease with increasing $\langle N_{\text{part}} \rangle$ for a given $\Delta \phi$ window, as expected. The $p_t$ correlations multiplied by $\langle N_{\text{part}} \rangle^2$ [Fig. 6(c) for Cu + Cu 200 GeV and Fig. 6(d) for Cu + Cu 62.4 GeV] seem to increase and then saturate with increasing $\langle N_{\text{part}} \rangle$.

D. $p_t$ dependence

Figure 7 shows the correlations as a function of collision centrality for different $p_t$ regions in Cu + Cu collisions at (a) $\sqrt{s_{NN}} = 200$ and (b) 62.4 GeV. The different $p_t$ ranges used are shown. These $p_t$ ranges are chosen to demonstrate the dependence of the correlations among tracks sets at lower $p_t$, at higher $p_t$, and in a set where all available $p_t$ values are included. The data points for $p_t$ ranges (in GeV/c), 0.15–0.5, 0.5–2.0, 0.15–0.35, and 0.35–2.0, are shifted by one unit in $\langle N_{\text{part}} \rangle$.

The $p_t$ correlation is maximum (minimum) for charged particles whose $p_t$ is in $0.15$–$2.0$ GeV/c ($0.15$–$0.35$ GeV/c). The $p_t$ correlation values are small and fairly independent of $p_t$ if a lower $p_t$ bound for the particles studied is fixed at 0.15 GeV/c and the upper $p_t$ bound is progressively increased up to 0.50 GeV/c. When the analysis is carried out by keeping the higher $p_t$ bound fixed at 2.0 GeV/c and subsequently...
decreasing the lower \( p_t \) bound to 0.15 GeV/c, the correlation values are found to increase.

Figure 8 shows the variation of \( p_t \) correlations as a function of \( \langle N_{\text{part}} \rangle \) for different \( p_t \) windows as calculated using the (a) AMPT (string melting), (b) UrQMD, and (c) HIJING (no jet quenching) model calculations for Cu + Cu collisions at 200 GeV. The AMPT calculations show \( p_t \) correlations that are similar to those observed in data for corresponding variations in the \( p_t \) windows. The trend of the correlation values shown by both UrQMD and HIJING is similar to what is seen in the data for the low-\( p_t \) windows where the lower bound is fixed at 0.15 GeV/c and the upper bound is increased from 0.35 GeV/c to 0.50 GeV/c. However, for UrQMD, if the higher \( p_t \) bound is fixed at 2.0 GeV/c and the lower \( p_t \) bound is subsequently decreased to 0.15 GeV/c, \( p_t \) correlation values remain similar. For the same case, HIJING shows a decrease in \( p_t \) correlation values when the lower \( p_t \) bound is decreased to 0.15 GeV/c. This is just the opposite of what is observed in data as seen in Fig. 7.

Because correlations are calculated for different \( p_t \) ranges, the \( p_t \) acceptance effect on the observed \( p_t \) correlations, is examined. The correlation values in different \( p_t \) ranges may depend on the \( p_t \) range size and on the fluctuations in the \( p_t \) spectrum slope in that \( p_t \) range. It is, therefore, important to see the effect of slope fluctuations on the correlation values in different \( p_t \) ranges. The \( p_t \) correlations can be formulated in terms of the fluctuations in the inverse slope parameter (effective temperature) by the following relation [17]:

\[
\langle \Delta p_t \Delta p_t \rangle \approx \left[ \frac{d\langle p_t \rangle}{dT} \right]^2 \Delta T^2, \tag{7}
\]

where \( \Delta T^2 \) describes the fluctuation in the inverse slope parameter. The dependence of \( \langle p_t(T) \rangle \) can be obtained from the function that describes the inclusive uncorrected \( p_t \) spectrum for the desired \( p_t \) range in the following manner. Figure 9 (top panel) shows the measured inclusive \( p_t \) spectrum for 0%-10% collision centrality in Cu + Cu collisions at 200 GeV. The dashed line represents the exponential fit of the form \( F(p_t) = A e^{-a/T} \) that is fit to these measurements for the \( p_t \) range 0.35–2.0 GeV/c. The expressions for \( \langle p_t \rangle \) and \( d\langle p_t \rangle/dT \) can be obtained using the following relation:

\[
\langle p_t \rangle = \frac{\int_a^b p_t^2 F(p_t) dp_t}{\int_a^b p_t F(p_t) dp_t}, \tag{8}
\]

which gives

\[
\langle p_t \rangle = 2T + \frac{a^2 e^{-a/T} - b^2 e^{-b/T}}{(a + T)e^{-a/T} - (b + T)e^{-b/T}}. \tag{9}
\]

Here, \( a \) and \( b \) are the lower and upper limits of a given \( p_t \) range, respectively. The derivative of \( \langle p_t \rangle \) with respect to \( T \) is obtained as

\[
\frac{d\langle p_t \rangle}{dT} = 2 - \frac{Ae^{-(a+b)/T} + a^2 e^{-a/T} + b^2 e^{-b/T}}{[(a + T)e^{-a/T} - (b + T)e^{-b/T}]^2}. \tag{10}
\]
where

$$A = \frac{ab(b-a)^2}{T^2} + \frac{(b^2-a^2)(b-a)}{T} - (a^2 + b^2). \quad (11)$$

Using the lower and upper limits of a given $p_t$ range, and the corresponding $T$ from the spectrum fit for each $p_t$ range and collision centrality, $(d\langle p_t \rangle/dT)^2$ are obtained for every $p_t$ range in each centrality.

Figure 9 (bottom panel) shows the measured two-particle $p_t$ correlations scaled by $(d\langle p_t \rangle/dT)^2$ vs $\langle N_{part} \rangle$ for different $p_t$ ranges in Cu + Cu 200 GeV. The data points for $p_t$ ranges (in GeV/c), 0.4–0.8, 0.5–2.0, 1.2–1.6, and 0.35–2.0, are shifted by one unit in $\langle N_{part} \rangle$ for clarity. The scaled $p_t$ correlations for different $p_t$ ranges become similar and show little dependence on the collision centrality. This study seems to suggest that the difference in the $p_t$ correlations for different $p_t$ ranges may due to the fluctuations in slope of the $p_t$ spectrum in those $p_t$ ranges.

V. SYSTEMATIC UNCERTAINTIES

Systematic errors on the mean ($\mu$) and standard deviation ($\sigma$) in the $\langle p_t \rangle$ distributions (discussed in Sec. III), and $p_t$ correlations (discussed in Sec. IV) are mainly evaluated by varying the different cuts used in the analysis, redoing the analysis using these changed cuts and determining the resulting changes in the values of $\mu$, $\sigma$, and the $p_t$ correlations. The difference is taken as the systematic error due to a particular analysis cut. The resulting systematic uncertainties, described below, are shown in Tables III and IV as a percentage of the result ($\mu$, $\sigma$, and the $p_t$ correlations) for various centralities for Cu + Cu collisions at both 62.4 and 200 GeV.

To study the effect of the $z$-vertex ($V_z$) cut, the $V_z$ acceptance is increased to $\pm 50$ cm from the default value of $\pm 30$ cm. No change in $\mu$ or $\sigma$ or in the $p_t$ correlations is observed when using the wider $V_z$.

The effect of the cuts used to suppress background tracks is studied by changing the DCA cut from the default, DCA $< 1$ cm, to DCA $< 1.5$ cm and separately, changing the required number of fit points along the track, $N_{Fit}$. from the default $N_{Fit} > 20$ to $N_{Fit} > 15$. The resulting systematic errors due to these changes are listed in Tables III and IV in the columns labeled “DCA” and “$N_{Fit}$.”

The effect of the size of the centrality bin on the $p_t$ correlations is addressed by fitting $\langle \langle p_t \rangle \rangle$ as a function of $\langle N_{ch} \rangle$ (see Sec. IV). To determine the systematic uncertainty associated with this process, different polynomial functions are used to fit $\langle \langle p_t \rangle \rangle$ vs $\langle N_{ch} \rangle$. The systematic errors associated with this correction are listed in Table IV in the columns labeled “Poly.”

The systematic uncertainty on the $p_t$ correlations that may be associated with the application of the low-$p_t$ cut is estimated by removing this $p_t$ cut in the HIJING [41] model calculations. The estimated systematic errors are shown in Table IV in the columns labeled “Low $p_t$.”

The $p_t$ correlations may also include short range correlations such as Coulomb interactions and Hanbury Brown-Twiss (HBT) correlations. These correlations usually dominate among pairs of particles having relative transverse momentum less than 100 MeV/c. The effect of these short-range correlations on the measured $p_t$ correlations is seen by calculating $p_t$ correlations after removing the pairs of particles with relative momentum $(p_t - p_t)$, less than 100 MeV/c. The $p_t$ correlations are reduced by a maximum of 6% when short-range correlations are excluded.

The $p_t$ correlations also include the contributions from resonance decays and charge ordering. These correlations are obtained for pairs of particles having like (+ + or --) and unlike (+ -) charges with respect to inclusive charged particles. A maximum of 15% decrease in the correlations is observed for pairs of particles with like charges and about 12% increase is observed for pairs with unlike charges with respect to the correlations for inclusive charged particle pairs for Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ GeV and 200 GeV.

VI. SUMMARY

We have reported measurements of $p_t$ fluctuations in Cu + Cu collisions in the STAR detector at RHIC for $\sqrt{s_{NN}} = 62.4$ and 200 GeV, and compared with Au + Au collisions at the same energies to investigate the system size dependence. The dynamical $p_t$ fluctuations are observed by comparing data to mixed events in both Cu + Cu and Au + Au collisions at
TABLE III. Systematic errors on $\mu$ and $\sigma$ in eventwise $\langle p_t \rangle$ distributions as described in Sec. III for various collision centralities in Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV.

| % cross section | Cu + Cu 62.4 GeV | Cu + Cu 200 GeV |
|-----------------|------------------|------------------|
|                 | DCA $\mu$ (%)    | $N_{\text{Fit}}$ $\mu$ (%) | DCA $\sigma$ (%) | $N_{\text{Fit}}$ $\sigma$ (%) | DCA $\mu$ (%) | $N_{\text{Fit}}$ $\mu$ (%) | DCA $\sigma$ (%) | $N_{\text{Fit}}$ $\sigma$ (%) |
| 0–10            | 3.6              | 0.4              | 7.9             | 1.0             | 3.4              | 0.24             | 5.7             | 1.2             |
| 10–20           | 3.6              | 0.4              | 7.1             | 1.0             | 3.3              | 0.23             | 5.2             | 1.2             |
| 20–30           | 3.6              | 0.4              | 6.6             | 1.0             | 3.3              | 0.23             | 5.2             | 1.1             |
| 30–40           | 3.6              | 0.4              | 6.2             | 1.0             | 3.3              | 0.20             | 4.7             | 1.2             |
| 40–50           | 3.6              | 0.4              | 6.0             | 1.0             | 3.2              | 0.20             | 4.9             | 1.1             |
| 50–60           | 3.6              | 0.4              | 6.0             | 1.0             | 3.2              | 0.22             | 4.4             | 1.2             |

These two beam energies. Moreover, for similar mean number of participating nucleons, the $p_t$ fluctuations are observed to be comparable for the Cu + Cu and Au + Au systems, suggesting that the system size has little effect. In addition, $p_t$ correlation measurements for Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ and 200 GeV are compared with the published Au + Au measurements. For both Cu + Cu and Au + Au systems, the $p_t$ correlation decreases with increasing $\langle N_{\text{part}} \rangle$ at both beam energies. The dilution of the $p_t$ correlations with increasing $\langle N_{\text{part}} \rangle$ could be due to the decrease in correlations that are dominated by pairs of particles that originate from the same nucleon-nucleon collision. A similar observation is found with other fluctuation and correlation observables such as $K/\pi$ [37] and net charge [43].

The $p_t$ correlations are found to scale with number of participating nucleon pairs for $\langle N_{\text{part}} \rangle > 100$ (when the system size is larger than that of central Cu + Cu collisions). This might indicate the onset of thermalization [26], the onset of jet quenching [3,11], or the saturation of transverse flow in central collisions [38]. The square root of the $p_t$ correlations normalized by eventwise average transverse momentum for Cu + Cu and Au + Au collisions is similar for systems with similar $\langle N_{\text{part}} \rangle$ and is independent of the beam energies studied.

The results described above are compared to predictions from several relevant model calculations. The transport-based UrQMD model calculations are found to have a better quantitative agreement with the measurements compared to models which incorporate only jet-like correlations as in HIJING. HIJING gives similar dependence on $\langle N_{\text{part}} \rangle$, but underpredicts the magnitude. Inclusion of the jet-quenching effect in HIJING leads to a smaller value of the correlations in central collisions. A multiphase transport model calculation incorporating coalescence as a mechanism of particle production also compares well with data for central collisions.

When studying the $p_t$ correlations for different $p_t$ intervals, the correlations appear to be small and fairly independent of $p_t$ interval, if the lower $p_t$ bound is fixed at 0.15 GeV/c and the higher $p_t$ bound is progressively increased up to 0.50 GeV/c. This suggests that correlations are weak for low-$p_t$ particles. This low-$p_t$ trend observed in the data is also seen in UrQMD, AMPT, and HIJING models. When the analysis is carried out keeping the higher $p_t$ bound fixed at 2.0 GeV/c and progressively decreasing the lower $p_t$ bound to $p_t = 0.15$ GeV/c, the correlation values in data are found to increase. This suggests that high $p_t$ particles are more correlated with low-$p_t$ particles. The AMPT model shows a rather similar variation of $p_t$ correlations for different $p_t$ intervals, as observed in data. The UrQMD model calculations, however, show no such variations in correlations for the different $p_t$ intervals with higher $p_t$ bound fixed at 2.0 GeV/c. Finally, it is noted that the HIJING model calculations give $p_t$ correlations that decrease with a decrease in the lower $p_t$ bound for intervals with fixed higher $p_t$ (=2.0 GeV/c) bound, i.e., opposite to what is observed in data. Regarding the changes in $p_t$ correlations in different $p_t$ intervals, it is found that the resultant fluctuations after considering event-by-event variation in the slope of the $p_t$ spectra for different $p_t$ bins are all of similar order.

TABLE IV. Systematic errors on $p_t$ correlations as described in Sec. IV for various collision centralities in Cu + Cu collisions at $\sqrt{s_{NN}} = 62.4$ GeV and 200 GeV.

| % cross section | Cu + Cu 62.4 GeV | Cu + Cu 200 GeV |
|-----------------|------------------|------------------|
|                 | DCA $p_t$ (%)    | $N_{\text{Fit}}$ $p_t$ (%) | Low $p_t$ (%) | DCA $p_t$ (%)    | $N_{\text{Fit}}$ $p_t$ (%) | Low $p_t$ (%) |
| 0–10            | 30               | 1.4              | 1.9             | 7.2             | 16               | 0.05             | 1.9             | 22             |
| 10–20           | 23               | 0.8              | 3.6             | 13.1            | 13               | 0.09             | 3.6             | 3.2             |
| 20–30           | 18               | 0.6              | 1.9             | 3.4             | 13               | 1.1              | 1.9             | 12.3            |
| 30–40           | 17               | 1.0              | 0.004           | 9.0             | 8                | 1.2              | 0.004           | 9.7             |
| 40–50           | 19               | 3.0              | 0.009           | 1.0             | 10               | 2.0              | 0.009           | 8.4             |
| 50–60           | 20               | 3.6              | 0.009           | 4.0             | 7                | 5.0              | 0.009           | 8.3             |
The variation of $p_t$ correlation with the change in the accepted range of pseudorapidity and azimuthal angle of the produced particles, are also shown. The correlation values increase when the $\eta$ and the $\phi$ acceptance are reduced.

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