The Simplest Memristor Circuit With Hyperchaos

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In recent years, with the in-depth study of the memristor, meminductor, and memcapacitor, the fourth basic element has been developed vigorously. The chaotic circuit including the meminductor, memcapacitor, and memristor is designed in this study. The equation of state for the chaotic system is obtained according to Kirchhoff's volt–current law, and the mathematical model of the chaotic system is obtained through dimensionless processing. The stability of the equilibrium point is analyzed in detail, and the dynamic behaviors of the system are analyzed by traditional methods such as LEs and bifurcation diagram. Moreover, some special phenomena exist in the system, such as state transition and coexistence of attractors. Finally, the circuit is implemented by DSP to prove the realizability of chaotic circuit.

Keywords: memristor, meminductor, memcapacitor, coexisting attractors, state transition, DSP implementation

INTRODUCTION

A chaotic system is a kind of complex nonlinear dynamic system, and its motion has pseudo-randomness. The orbit moves in a specific range but never repeats. Chaos is often described as a specific phenomenon with an infinite period or a phenomenon similar to random behavior. According to the growing understanding of chaos, people found that chaos includes not only integer-order chaotic system but also fractional-order chaotic system [1–7]. In addition, people usually study chaos by constructing chaotic circuits. The nonlinear element is an important part of the nonlinear system.

The memristor is a kind of nonlinear element [8]. Professor Chua presented a special circuit element and suggested that it could be used to describe the relationship between charge value and magnetic flux in 1971 and it is called a memristor [9]. From then on, Professor Chua proposed the concept of memristor for several decades, and no memristor element has been found in practice. So research on the fourth basic element has been stalled. Until 2008, the HP Laboratory in the United States claimed to have completed the hardware realization of memristor components on the nanoscale for the first time, which eventually led to booming research on the fourth type of components [10, 11]. Many research studies on chaotic circuits are carried out from this [12–16]. However, at present, because the hardware implementation of the memristor in the real sense can only be completed at the laboratory level, the application research of the memristor is mainly based on its mathematical model or the circuit equivalent model.

Through continuous research on the memristor, in 2009, Professor Chua presented the meminductor and memcapacitor, two memory elements, which further deepen the research on nonlinear systems. Although the basic principles of meminductor and memcapacitor components have been understood, there is no material that can be used to manufacture these two basic components in nature, so the hardware implementation of the meminductor and memcapacitor is still at a standstill until now. However, due to its unique memory
characteristics, many theoretical analyses and research studies on meminductor and memcapacitor components have been completed. The chaotic circuits based on the meminductor and memcapacitor are rarely reported [17–20].

Because of their distinctively dynamic characteristics, the memristor, meminductor, and memcapacitor have been used in chaotic systems. In 2008, a memristor was used to replace Chua’s diode to design the chaotic system, and numerical simulation analysis and circuit implementation were carried out [21]. In 2012, Professor Chua first proposed a simple-series chaotic circuit based on a memristor and implemented it. The circuit consists only of a memristor, an inductor, and a capacitor in series [22]. In 2013, Professor Xu modified the simplest chaotic circuit. By connecting the inductor, memristor, and capacitor in parallel, he proposed a minimalist parallel chaotic circuit and simulated it [23]. In 2019, Professor Yuan constructed the simplest parallel chaotic circuit by connecting the memcapacitor, meminductor, and memristor in parallel. Its dynamic characteristics were not only analyzed but also the circuit simulation was carried out [24]. The chaotic system based on the memristor and other memory elements has better application in a neural network, chaotic secure communication, and image encryption due to its excellent dynamic characteristics [25–39].

In this study, a chaotic system including the meminductor, memcapacitor, and memristor is proposed. Because of the special dynamic characteristics of the memristor, meminductor, and memcapacitor, compared with the general chaotic oscillator, it has more dynamic characteristics [40–43]. Finally, digital circuits are less affected by the environment and have greater flexibility in parameter changes. Therefore, a complete set of dynamic analyses and implementation of a chaotic oscillator is carried out by DSP in this study to prove the realizability of the circuit [44–52].

The rest of the study follows according to the abovementioned background. In the second section, the model of the memcapacitor, meminductor, and meminductor is presented. In the third section, the state equation is determined by the constructed chaotic circuit, the stability of the equilibrium point is analyzed, and the dynamical characteristics of the system are analyzed through the traditional way. In the fourth section, the circuit is implemented by DSP. In the fifth section, the relevant work of this study is summarized.

MODELS OF THE MEMCAPACITOR, MEMINDUCTOR, AND MEMRISTOR

Model of the Memristor

This study uses the model of the classic memristor proposed by Professor Chua [53]. The equation of state is shown below:

\[
\begin{align*}
V_M &= a(y^2 - 1)i_M \\
y' &= i_M - by - i_M y
\end{align*}
\]  

(1)

In the equation, \(i_M\) represents the current of the memristor, \(V_M\) represents the voltage of the memristor, \(b\) and \(a\) represent the parameters, and \(y\) represents the state variables of the memristor.

An AC power supply with a frequency of 10 Hz is assumed and an effective value of 10 A is input at both ends of the memristor. Through numerical simulation of the memristor, we can obtain its \(v-i\) memory curve, as shown in Figure 1A. The simulation results show that its characteristic curve is a compact “8” hysteretic curve. As the frequency increases, the side lobe area of the characteristic curve decreases. This is consistent with the basic characteristics of the memristor proposed by Professor Chua.

Model of the Memcapacitor

By professor Chua’s definition of the memcapacitor, it is a passive memory element [54]. According to the definition of the memcapacitor, the current passing through it can be expressed as \(i\), the charge gathered at both ends of the memcapacitor can be expressed as \(q\), and the time integral of charge quantity \(q\) can be expressed as \(\sigma\). So, the state equation of the memcapacitor element is shown as follows:

\[
\begin{align*}
v(t) &= C_M^{-1}(\sigma)q(t) \\
C_M^{-1}(\sigma) &= c + d \cos(\sigma) \\
\sigma &= \int_{t_0}^{t} q(\tau)d\tau \\
q &= \int_{t_0}^{t} i(\tau)d\tau
\end{align*}
\]  

(2)

For the model of the memcapacitor mentioned above, when the input of the memcapacitor is an AC power supply with a frequency of 10 Hz and an effective value of 2A, the curve of the dynamic characteristic of the memcapacitor can be obtained through numerical simulation, as shown in Figure 2. This is a compact hysteresis curve with a shape similar to an inclined “8”, and the side lobe area decreases with increasing frequency. This is consistent with the basic properties of memcapacitors.

Model of the Meminductor

By professor Chua’s definition of the meminductor [54], its model used in this study is as follows:

\[
\begin{align*}
i(t) &= L_M^{-1}(\rho)\phi(t) \\
L_M^{-1}(\rho) &= e + gp \\
\rho &= \int_{t_0}^{t} \phi(\tau)d\tau
\end{align*}
\]  

(3)

The \(\rho\) in the equation is the integral of magnetic flux \(\varphi\), where \(e\) and \(g\) represent the internal parameters of the meminductor.

A sinusoidal signal with a magnetic flux of 10 Wb and a frequency of 5 Hz is applied at both ends of the meminductor, and the characteristic curve of the meminductor element \(\Phi-i\) is shown in Figure 3A. The curve of the meminductor is also a slanted hysteresis curve similar to “8”. Through numerical
simulation, it was found that the sidelobe area of the characteristic curve of the meminductor gradually decreased with the increase of input frequency, which was consistent with the dynamic characteristics of the meminductor proposed by Professor Chua.

A NEW SIMPLE CHAOTIC OSCILLATOR

A New Chaotic Oscillator

In this circuit, there are three nonlinear elements, namely, an independent charge-controlled memcapacitor, a charge-
obtained as follows:

\[
\begin{align*}
\dot{x} &= -(e + gu)z - a(y^2 - 1)(c + d \cos w)x \\
\dot{y} &= (c + d \cos w)x - by - (c + d \cos w)xy \\
\dot{z} &= (c + d \cos w)x \\
\dot{u} &= z \\
\dot{w} &= x
\end{align*}
\]

(5)

When the initial conditions are set as \((1, 40, 1.5, 20, -15)\) and the parameters are set as \(b = 20, a = 49, g = 2, e = 100, c = 0.2,\) and \(d = -0.02,\) the phase diagram simulated by MATLAB is expressed in Figure 5.

**Equilibrium Point Set and Stability**

The calculation method of divergence of the chaotic system is shown as

\[
\nabla V = \frac{\partial \dot{x}}{\partial x} + \frac{\partial \dot{y}}{\partial y} + \frac{\partial \dot{z}}{\partial z} + \frac{\partial \dot{u}}{\partial u} + \frac{\partial \dot{w}}{\partial w} = -a(y^2 - 1)(c + d \cos w) - b - (c + d \cos w)x. 
\]

(6)

For the parameters set as \(a = 49, b = 20, g = 2, e = 100, c = 0.2,\) and \(d = -0.02,\) the divergence of the system is calculated to be \(-16,881.\) This means that the system can produce chaos.

Let the system state variable \(\dot{x} = \dot{y} = \dot{z} = \dot{u} = \dot{w} = 0,\) we can obtain the calculation result as follows:

\[
\begin{align*}
-(e + gu)z - a(y^2 - 1)(c + d \cos w)x &= 0 \\
(c + d \cos w)x - by - (c + d \cos w)xy &= 0 \\
(c + d \cos w)x &= 0 \\
z &= 0 \\
x &= 0
\end{align*}
\]

(7)

Through calculation, the equilibrium point of the system is obtained as \((0, 0, 0, n, m).\) It shows that the system had an infinite number of equilibrium points. According to Eq. 7, the Jacobian matrix \(J_E\) of the system can be obtained.
FIGURE 6 | Bifurcation diagram and LEs with parameter \(a\), (A) LEs, and (B) bifurcation diagram.

FIGURE 7 | Bifurcation diagram and LEs with parameter \(b\), (A) LEs, and (B) bifurcation diagram.

FIGURE 8 | Bifurcation diagram and LEs with parameter \(g\), (A) LEs, and (B) bifurcation diagram.
and \(-15\). Let the parameters be obtained through the Jacobian matrix of the system. Therefore, the characteristic polynomial of the system can be expressed in the form:

\[ \lambda^5(\lambda^3 + m_1\lambda^2 + m_2\lambda + m_3) = 0, \] (9)

where \(m_1 = b-a(c+dcosm)\), \(m_2 = [(c + dcosm)(c + gn)-ab(c + dcosm)]\), and \(m_3 = b((c + dcosm)(c + dn))\).

Equation 9 means system (5) has three non-zero eigenvalues and one zero eigenvalue, where \(m_1, m_2, \text{ and } m_3\) are coefficients. By the Routh–Hurwitz criterion, system (5) is stable if \(m_1 > 0, m_2, m_2m_2m_2 > 0, \text{ and } m_3(m_2m_2m_2) > 0\). At least one of the eigenvalues of the chaotic systems is positive, so the \(m_1, m_1m_2m_2, \text{ and } m_3\) should be not all positive. So, we could set \(O\) such as \(O_1(0, 0, 0, 20, -15)\). Let the parameters be \(a = 49, b = 20, e = 100, c = 0.2,\) and \(d = -0.02,\) and we can get \(m_1 = 9.4552 > 0, m_2 = -180.768 > 0, m_3 = 602.56 > 0, m_1m_2m_2 < 0, m_3(m_2m_2m_2) < 0\) and \(\lambda_1 = \lambda_2 = 0, \lambda_3 = -20, \lambda_4 = 5.2722 + 1.5266i, \lambda_5 = 5.2722 - 1.5266i\). This means that the system is unstable, and it is possible for such a system to produce chaos.

The Impact of the Parameters

To display the dynamical behaviors of the system designed by us more directly, we use the bifurcation diagram and LEs to study the dynamic behaviors of the system when parameter \(a\) changes. Other parameters of the chaotic system are set as \(d = -0.02, g = 2\), \(e = 100\), \(b = 20\), and \(c = 0.2\), and the initial condition is \(1, 40, 1.5, 20, \text{ and } -15\). The calculation results are as follows Figure 6.

According to the LEs and bifurcation diagram, we can understand that the bifurcation diagram and LEs can correspond to each other. According to the definition of LEs, the system has two positive Lyapunov exponents in a certain parameter range, which shows that the system is a hyperchaotic system. According to the bifurcation diagram, with the change of parameter \(a\), the system enters into a chaotic state by means of period-doubling bifurcation.

To study the dynamic behaviors of the simple system parameter \(b\) is treated as a variable. Other parameters are set as \(a = 49, g = 2, e = 100, c = 0.2,\) and \(d = -0.02\), and the initial values are \(1, 40, 1.5, 20, \text{ and } -15\). The results of numerical simulation are expressed in Figure 7.

By observing the LEs, we can see that the bifurcation diagram and LEs agree perfectly. From LEs, we can find simply that the system not only has a chaotic state but also has a hyperchaotic state. According to the bifurcation diagram, when the parameter \(b\) increases, the system enters into chaos by period-doubling bifurcation.

When the system parameters \(a = 49, b = 20, e = 100, c = 0.2,\) and \(d = -0.02\) and the initial values are \(1, 40, 1.5, 20, -15\), just the parameter \(g\) is changed. The bifurcation diagram and LEs are expressed in Figure 8.

By the analysis of LEs, we can know that when the parameter \(g\) increases, the system changes frequently between periodic state, chaotic state, and hyperchaotic state. Also, the system is produced by a counter-periodic doubling of the chaotic state. The bifurcation diagram and LEs agree well.
Complexity Analysis

The chaotic state and hyperchaotic state are the most valuable intervals of a chaotic system. When the system is chaotic or hyperchaotic, the sequence generated by the system has high pseudo-randomness, which makes the system have good anti-decoding performance. When the system shows higher complexity, its dynamic performance is also superior. So, in image encryption, people mostly choose the parameter range with higher complexity. To further understand the dynamic behaviors, two complexity algorithms $C_0$ and $SE$ (spectral entropy) are used to analyze the system complexity. The results show that the $SE$ and $C_0$ algorithms reflect the
dynamic behaviors. The initial values are set as 1, 40, 1.5, 20, and -15 and the system parameters $b = 20$, $e = 100$, $c = 0.2$, $d = -0.02$, and $a = 20$ are kept unchanged. Only the system parameters $a$ and $g$ are changed. As system parameters $a$ and $g$ change, the system parameters $a = 49$, $b = 20$, $e = 100$, $c = 0.2$, $d = -0.02$, and $g = 2$, and simulation step $t = 0.001s$. In addition, let the initial condition be $1, 20, z_0, 20, w_0$. When the initial value is changed, the results are shown in Figure 13A.

Coexistence of Attractors
Coexistence of attractors is a special phenomenon of chaotic systems [55–57]. For the chaotic circuit system with the memristor, meminductor, and memcapacitor, let $a = 49$, $b = 20$, $e = 100$, $c = 0.2$, $d = -0.02$, $g = 2$, and simulation step $t = 0.001s$. When the initial value is changed, the results are shown in Figure 13:

DSP IMPLEMENTATION
Because DSP implementation has strong anti-interference ability, the parameters in the system are also better controlled. The DSP is called

![Diagram](image)

**FIGURE 14** | Flow chart.

**FIGURE 15** | Experimental results of DSP implementation. (A) $x-y$ plane; (B) $x-w$ plane.
digital signal processor. Digital signal processing is the use of computers or special processing equipment in the digital form of signal acquisition, transformation, filtering, valuation, enhancement, compression, recognition, and other processing in order to get the signal form that meets people’s needs. We choose to use the DSP to achieve the chaotic system. However, because of the limited precision of DSP hardware implementation, we choose the TMS320F28335 chip so as to meet the requirements of system precision. To make the oscilloscope capture the image more easily, we use a D/A converter to convert the DSP-generated sequence into the analog sequence and then transmit the signal to the oscilloscope (UTD7102H) through the D/A converter (8552). The flow chart of DSP implementation is shown in Figure 14.

Let its parameters be \( a = 49, b = 20, c = 100, d = -0.02, \) and \( g = 2. \) The initial value is \( (1, 40, 1.5, 20, -15). \) First, the parameters and initial value are set and then iterative calculation is started. The data generated by each iteration are stored using stack techniques to avert corruption. The results of DSP implementation are expressed in Figure 15.

Hardware such as oscilloscope, D/A converter, and F28335 chip used in DSP implementation are shown in Figure 16. The results of DSP parameters and initial value are set and then iterative calculation.

### CONCLUSION

In this study, the circuit with the memcapacitor, memristor, and meminductor is constructed. The study not only introduces the model of the meminductor, memcapacitor, and memristor but also obtains the dynamics equation of the system by Kirchhoff's voltage–current law. The stability of the equilibrium point is analyzed by means of traditional dynamics. Through the analysis of LES, complexity, and bifurcation diagram, it is found that when the initial conditions and parameters change, the chaotic system shows complex dynamical behavior. Also, the system has not only a chaotic state but also a hyperchaotic state. In addition, some special phenomena such as state transition and coexistence of attractors are found in the analysis of the systems. Finally, the DSP is used to realize the chaotic circuit, and the simulation diagram in the DSP is highly consistent with the results of numerical simulation. The rich dynamic characteristics show that it can be used in chaotic image encryption.

### DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Materials, further inquiries can be directed to the corresponding author.

### AUTHOR CONTRIBUTIONS

XL designed and carried out experiments, analyzed data, and wrote the manuscript. JW made the theoretical guidance for this study. All authors reviewed the manuscript.

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