Measurement of the charge asymmetry in $B^\pm \rightarrow \phi K^\pm$ and search for $B^\pm \rightarrow \phi \pi^\pm$ decays
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LHCb Collaboration

1. Introduction

The weak-interaction $B^{\pm} \to \phi K^{\pm}$ decay is governed by the $b \to s\bar{s}\bar{s}$ transition. In the Standard Model (SM), it can only occur through loop diagrams (see Fig. 1), leading to a branching fraction of order $10^{-5}$ [1]. Because the dominant amplitudes have similar weak phases, the CP-violating charge asymmetry, defined as

$$A_{CP}(B^{\pm} \to \phi K^{\pm}) = \frac{B(B^{-} \to \phi K^{-}) - B(B^{+} \to \phi K^{+})}{B(B^{-} \to \phi K^{-}) + B(B^{+} \to \phi K^{+})},$$

is predicted to be small in the SM, typically 1–2% with uncertainties of a few percent [2,3]. A significantly larger value would signal interference with an amplitude not described in the SM. The current experimental world average is $A_{CP}(B^{\pm} \to \phi K^{\pm}) = 0.10 \pm 0.04$ [1], dominated by a recent measurement from the BaBar Collaboration [4]. Large CP violation effects have been seen in some regions of the $B^{\pm} \to K^{\pm} K^{-} K^{+}$ phase space, but not around the $\phi$ resonance [5].

The $B^{\pm} \to \phi \pi^{\pm}$ decay is another flavoured-change neutral current process, driven by the $b \to d\bar{s}\bar{s}$ quark-level transition (see Fig. 1). The high suppression, due to the tiny product of the Cabibbo–Kobayashi–Maskawa matrix elements [6,7] and to the Okubo–Zweig–Iizuka (OZI) rule [8–10] associated with the creation of the colourless $s\bar{s}$ pair forming the $\phi$ meson, makes this rare loop decay a sensitive probe of the SM. Indeed, even a small non-SM amplitude, e.g. from R-parity violating supersymmetry [11], may dominate over the SM contribution.

The current SM prediction for the $B^{\pm} \to \phi \pi^{\pm}$ branching fraction suffers from uncertainties originating from the naive factorization approach, radiative corrections, calculation of the long-distance contribution (e.g. $B \to K K^*$ rescattering), and $\omega$–$\phi$ mixing [12]. The latter is the main source of uncertainty. The physical $\omega$ and $\phi$ meson states do not coincide exactly with the ideal $|u\bar{d}| + |d\bar{u}|/\sqrt{2}$ and $|s\bar{s}|$ states, respectively. They appear to be mixtures of these two states characterized by a small mixing angle $\delta_{V}$ [13,14], which depends on the magnitude of SU(3) symmetry breaking and can be determined in the framework of chiral perturbation theory. However, more sophisticated treatments based on the full $\rho^0$–$\omega$–$\phi$ mixing scheme suggest that $\delta_{V}$ is mass dependent, i.e. takes different values at the $\omega$ and $\phi$ masses [15,16]. In the QCD factorization approach, the $B^{\pm} \to \phi \pi^{\pm}$ branching fraction is predicted to be in the range $(5 \times 10^{-4}) \cdots (5 \times 10^{-1})$ [3] if $\omega$–$\phi$ mixing is neglected, but can be enhanced up to $6 \times 10^{-3}$ [12,17] depending on the value of $\delta_{V}$. However, the effect of $\omega$–$\phi$ mixing has not been observed in a recent search for $B^{0} \to J/\psi\phi$ [18]. Values of the $B^{\pm} \to \phi \pi^{\pm}$ branching fraction in excess of $10^{-3}$ would be indicative of non-SM physics.
The $B^\pm \to \phi \pi^\pm$ decay mode has not been observed yet. Currently, the most stringent experimental limit is $B(B^\pm \to \phi \pi^\pm) < 2.4 \times 10^{-7}$ at 90% confidence level (CL), obtained by the BaBar Collaboration [19].

This Letter presents a measurement of the $B^\pm \to \phi K^\pm$ charge asymmetry and a search for the $B^\pm \to \phi \pi^\pm$ decay mode with the LHCb detector. The results are based on a data sample collected during the 2011 pp run of the Large Hadron Collider at a centre-of-mass energy of 7 TeV, corresponding to an integrated luminosity of 1.0 fb$^{-1}$. The $\phi$ meson is reconstructed in the $K^+ K^-$ final state. We define the $\phi$ signal as any peaking component in the $K^+ K^-$ mass spectrum consistent with the known parameters of the $\phi$ resonance, without attempting a full amplitude analysis of the three-body $K^+ K^0$ and $K^+ K^- \pi^\pm$ final states. In order to suppress several systematic effects, the primary observables measured in this analysis are the difference of $CP$-violating charge asymmetries

$$\Delta A_{CP} \equiv A_{CP}(B^\pm \to \phi K^\pm) - A_{CP}(B^\pm \to J/\psi K^\pm),$$

and the branching fraction ratio $B(B^\pm \to \phi \pi^\pm)/B(B^\pm \to \phi K^\pm)$, which are then converted to results on $A_{CP}(B^\pm \to \phi K^\pm)$ and $B(B^\pm \to \phi \pi^\pm)$ using the best known values of $A_{CP}(B^\pm \to J/\psi K^\pm)$ [10,20] and $B(B^\pm \to \phi K^\pm)$ [1]. The choice of $B^\pm \to J/\psi K^\pm$ as reference channel and other features of the analysis follow the approach adopted in inclusive studies of $B^\pm \to K^+ K^- K^0$ decays with the same data set [5].

The two measurements are performed in a common analysis, i.e. they are based on identical event selections and data descriptions whenever possible. The observables are obtained from two-dimensional maximum likelihood fits to the unbinned $B^\pm$ and $\phi$ mass distributions of the reconstructed candidates, using parametric shapes with minimal dependence on simulation. The results of these fits were not examined until the entire analysis procedure was finalized.

2. Detector and data set

The LHCb detector [21] is a single-arm forward spectrometer covering the pseudorapidity range $2 < \eta < 5$, designed for the study of particles containing $b$ or $c$ quarks. The detector includes a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the pp interaction region, a large-area silicon-strip detector located upstream of a dipole magnet with a bending power of about 4 Tm, and three stations of silicon-strip detectors and straw drift tubes placed downstream. The combined tracking system provides a momentum measurement with a relative uncertainty that varies from 0.4% at 5 GeV/c to 0.6% at 100 GeV/c, and an impact parameter (IP) resolution of 20 $\mu$m for tracks with high transverse momentum ($p_T$). Charged hadrons are identified using two ring-imaging Cherenkov detectors [22]. Photon, electron and hadron candidates are identified by a calorimeter system consisting of scintillating-pad and preshower detectors, an electromagnetic calorimeter and a hadronic calorimeter. Muons are identified by a system composed of alternating layers of iron and multiwire proportional chambers. The direction of the magnetic field of the spectrometer dipole magnet is reversed regularly.

The trigger [23] consists of a hardware stage, based on information from the calorimeter and muon systems, followed by a software stage, which applies a full event reconstruction. The $B^\pm$ candidate decays considered in this analysis must belong to one of two exclusive categories of events, called TOS (triggered on signal) or TIS (triggered independently of signal). A TOS event is triggered at the hardware stage by one of the candidate’s final-state particles being compatible with a transverse energy deposit greater than 3.5 GeV in the hadron calorimeter. A TIS event does not satisfy the TOS definition and is triggered at the hardware stage by activity in the rest of the event. All candidates must pass a software trigger requiring a two-, three- or four-track secondary vertex with a large scalar sum of the transverse momentum of the tracks and a significant displacement from the primary pp interaction vertices (PVs). At least one track should have $p_T > 1.7$ GeV/c and $\chi^2_{IP}$ with respect to any PV greater than 16, where $\chi^2_{IP}$ is defined as the difference in $\chi^2$ of a given PV reconstructed with and without the considered track. A multivariate algorithm [24] is used for the identification of secondary vertices consistent with the decay of a $b$ hadron.

In the simulation, $pp$ collisions are generated using PYTHIA 6.4 [25] with a specific LHCb configuration [26]. Decays of hadronic particles are described by EVTGEN [27], in which final state radiation is generated using PHOTOS [28]. The interaction of the generated particles with the detector and its response are implemented using the GEANT4 toolkit [29] as described in Ref. [30].

3. Event selection and efficiency

The selections of $B^\pm \to \phi K^\pm$ and $B^\pm \to \phi \pi^\pm$ candidates are identical, except for the particle identification (PID) requirement on the charged hadron combined with the $\phi$ candidate, which is referred to as the bachelor hadron $h^\pm$ ($h^\pm = K^\pm$ or $\pi^\pm$). The other requirements are chosen to minimize the relative statistical uncertainty on the $B^\pm \to \phi K^\pm$ signal yield.

Only good quality tracks with $\chi^2_{IP} > 25$ and $p_T > 0.25$ GeV/c are used in the reconstruction. The $\phi$ meson candidates are reconstructed from two oppositely-charged tracks identified as kaons with the PID requirement DLL[KL] > 2, where DLL[KL] is the difference in log-likelihood between the kaon and pion hypotheses, as determined with the ring-imaging Cherenkov detectors in control samples of known particle composition [22]. The $\phi$ candidates are required to have $p_T > 2$ GeV/c, a total momentum, $p$, larger than 10 GeV/c and an invariant mass, $m_{KK}$, in the range 1.00–1.05 GeV/c$^2$. Bachelors, hadrons, reconstructed either as pions if DLL[KL] < −1 or kaons otherwise, are required to have $p > 10$ GeV/c and $p_T > 2.5$ GeV/c, and are combined with $\phi$ candidates to form $B^\pm \to \phi h^\pm$ candidates. These $h^\pm$ candidates are required to have $p_T > 2$ GeV/c, a three-track vertex $\chi^2$ per degree of freedom less than 9, and an invariant mass $m_{h^\pm K}$ in the range 5.0–5.5 GeV/c$^2$. Furthermore cos$\theta_p$ is required to be greater than 0.9999, where $\theta_p$ is the angle between the $B^\pm$ momentum vector and the vector joining the $B^\pm$ production vertex to the $B^\pm$ decay vertex. The production vertex is chosen as the PV for which the $B^\pm$ has the smallest $\chi^2_{IP}$.

Multiple candidates, occurring in 0.2% of the events, are removed by keeping the candidate with the smallest $B^\pm$ vertex $\chi^2$. The final data sample consists of 6251 $B^\pm \to \phi K^\pm$ candidates and 2169 $B^\pm \to \phi \pi^\pm$ candidates.

The PID performance is determined from a large and high-purity sample of pions from prompt $D^{*+} \to D^0 (K^- \pi^+) \pi^+$ and $D^{*-} \to \bar{D}^0 (K^+ \pi^-) \pi^-$ decays, as a function of $p$ and $\eta$. After reweighting this calibration sample to the same momentum and pseudorapidity distributions as for the bachelor pion in simulated $B^\pm \to \phi \pi^\pm$ decays, the efficiency of the PID requirement DLLK[KL] < −1 for the bachelor pion is measured to be 0.846 ± 0.011(stat) ± 0.020(syst), with a 5% kaon misidentification probability. All other efficiencies, which are slightly different for $B^\pm \to \phi \pi^\pm$ and $B^\pm \to \phi K^\pm$ decays due to their kinematic properties, are determined from simulation. The efficiency ratio

$$\frac{\epsilon(B^\pm \to \phi \pi^\pm)}{\epsilon(B^\pm \to \phi K^\pm)} = 0.762 \pm 0.031(\text{stat}) \pm 0.036(\text{syst})$$

(3)
is obtained, where the numerator is the total efficiency for a $B^\pm \rightarrow \phi \pi^\pm$ decay to be selected as a $B^\pm \rightarrow \phi \pi^\pm$ candidate and the denominator is the total efficiency for a $B^\pm \rightarrow \phi K^\pm$ decay to be selected either as a $B^\pm \rightarrow \phi K^\pm$ candidate or as a $B^\pm \rightarrow \phi \pi^\pm$ candidate. The statistical uncertainty arises from the size of the calibration and simulation samples, while the systematic uncertainty is the quadratic sum of contributions from the PID ($\pm 0.018$), the trigger ($\pm 0.008$), and other offline kinematic selection requirements ($\pm 0.030$).

4. Fit description

The observables of interest, namely the asymmetry between the $B^+ \rightarrow \phi K^-$ and $B^+ \rightarrow \phi K^+$ yields and the ratio between the $B^\pm \rightarrow \phi \pi^\pm$ and $B^\pm \rightarrow \phi K^\pm$ yields, are each determined from a two-dimensional unbinned extended maximum likelihood fit based on probability density functions (PDFs) of the $m_{KKh}$ and $m_{KK}$ masses. In each case, independent subsamples of events, each with either $B^+ \rightarrow \phi K^\pm$ candidates or $B^\pm \rightarrow \phi \pi^\pm$ candidates, are fitted simultaneously. For each subsample, the likelihood is written as

$$L = \exp \left( -\sum_j N_j \right) \prod_i \left( \sum_j N_j P_j \right).$$

where $N_j$ is the yield of fit component $j$, $P_j$ is the probability of event $i$ for component $j$, and the index $i$ runs over the $N$ events in the subsample. Except for the misidentified components described further below, the probabilities $P_j$ are given by the product of PDFs for the two $K^+ K^- h^\pm$ and $K^+ K^- \pi^\pm$ invariant masses, evaluated at the values $m_{KKh}^i$ and $m_{KK}^i$ of event $i$:

$$P_j = P_{KKh}^i (m_{KKh}^i) \cdot P_{KK}^i (m_{KK}^i).$$

This assumes that the two mass variables are independent, as supported by data and simulation studies. The correlation between $m_{KKh}$ and $m_{KK}$ is found to be less than 4%.

The description of the $m_{KKh}$ distributions involves a combination of three contributions: a signal peaking at the $B^\pm$ mass, a broad low-mass background with an end-point near 5150 MeV/$c^2$ due to partially-reconstructed $b$-hadron decays such as $B^0 \rightarrow \phi K^0_s$, and a linear background from random combinations. The peaking signal is modelled with a Crystal Ball function [31] modified such that both the upper and lower tails are power laws. The mean and the width $\sigma_B$ of the Crystal Ball function are free in the fit, while the tail parameters are determined from simulation. The partially-reconstructed background is described with an ARGUS function [32] convoluted with a Gaussian resolution function of the same $\sigma_B$ as the $B^\pm$ signal. The $m_{KK}$ distribution is described with two contributions: a peaking term centred on the $\phi$ mass, described with a relativistic Breit–Wigner function convoluted with a Gaussian resolution function of free width, and a linear term originating from nonresonant, $S$-wave, or random combinations of two kaons. The above three $m_{KKh}$ contributions and two $m_{KK}$ contributions lead to six components for each subsample: the $B^\pm \rightarrow \phi K^\pm$ signal, the nonresonant $B^\pm \rightarrow K^+ K^- h^\pm$ background, the partially-reconstructed $h$-hadron backgrounds with or without a true $\phi$ meson [for example $B^\pm \rightarrow \phi K^\pm \pi$, or $B^\pm \rightarrow K^* h_{\pi \pi}$, and the combinatorial backgrounds with or without a true $\phi$ meson. The nonresonant $B^\pm \rightarrow K^+ K^- h^\pm$ components include $b \rightarrow c$ decays, which are found to be negligible from simulation studies.

In addition, we consider components for the misidentified $B^\pm \rightarrow \phi K^\pm$ and $B^\pm \rightarrow K^+ K^- K^\mp$ decays in the $B^\pm \rightarrow \phi \pi^\pm$ sample, while misidentified $B^\pm \rightarrow \phi \pi^\pm$ and $B^\pm \rightarrow K^+ K^- \pi^\pm$ decays in the $B^\pm \rightarrow \phi K^\pm$ sample are negligible, and therefore ignored. For these two additional components, the $m_{KKh}$ PDF is conditional to the observable $\delta m = m_{KK} - m_{KKh}$, which is the mass difference under the two bachelor hadron mass hypotheses. The probabilities are written as

$$p_{j KK}^i = p_{KKh}^i (m_{KKh}^i) \cdot P_{KK}^i (m_{KK}^i),$$

where $p_{j KK}$ is the $m_{KK}$ PDF described above (representing either $\phi$ signal or background) and

$$p_{KKh}^i (m_{KKh}^i) \mid_{\delta m_i} = p_{KKh}^i (m_{KKh}^i) \cdot \delta m_i \mid_{\sigma_B \rightarrow \rho \delta m_i}. \quad (7)$$

Here $p_{KKh}$ is the $m_{KK}$ PDF of the $B^\pm \rightarrow \phi K^\pm$ signal, but with an increased $B^\pm$ mass resolution to account for the effects of the typically higher momentum of misidentified bachelor kaons. The parameter $\rho$ is multiplied here by the central value of a factor $\rho = 1.26 \pm 0.10$, determined from data as the ratio of the measured $m_{KK}$ resolutions of the $B^+ \rightarrow \phi K^+$ signal in the regions $-1 < \text{DLL}_{\pi} < -1$ and $\text{DLL}_{\pi} > 1$. The expression in Eq. (7) is equivalent to $p_{KKh}^i (m_{KKh}^i) \mid_{\delta m_i} \rightarrow \rho \delta m_i$, which means that the $B^\pm \rightarrow \phi K^\pm$ misidentified component in the $B^\pm \rightarrow \phi \pi^\pm$ sample would have a $B^\pm \rightarrow \phi K^\pm$ signal distribution if the correct mass was assigned to the bachelor kaon. The advantage of introducing the $\delta m$ observable is to connect the $B^\pm \rightarrow \phi K^\pm$ shapes in the $B^\pm \rightarrow \phi \pi^\pm$ and $B^\pm \rightarrow \phi K^\pm$ samples, thereby constraining the misidentified $B^\pm \rightarrow \phi K^\pm$ component in the $B^\pm \rightarrow \phi \pi^\pm$ sample using the large signal in the $B^\pm \rightarrow \phi K^\pm$ sample. This procedure allows to describe the misidentified component with the same parametric shape as the $B^\pm \rightarrow \phi \pi^\pm$ signal, and reduces the statistical uncertainty on the $B^\pm \rightarrow \phi \pi^\pm$ yield by a factor of two. However, this introduces a bias because the $\delta m$ distribution, which is not accounted for in the likelihood, is not the same for all components [33]. To reduce this bias, the $B^\pm \rightarrow \phi \pi^\pm$ sample is divided into four bins of $\delta m$, each with its own eight components. This procedure reduces the bias on the $B^\pm \rightarrow \phi \pi^\pm$ signal yield to a negligible level.

Other fit parameters that are common to the different subsamples are the $m_{KKh}$ end-point of the partially-reconstructed backgrounds, the peaking $m_{KK}$ PDF parameters for all components containing a $\phi$ meson, and the $m_{KK}$ slope of the nonresonant $B^\pm \rightarrow K^+ K^- h^\pm$ components. Finally, the ratio of the yield of the misidentified nonresonant $B^\pm \rightarrow K^+ K^- h^\pm$ component to the yield of misidentified $B^\pm \rightarrow \phi K^\pm$ background in the $B^\pm \rightarrow \phi \pi^\pm$ sample is constrained to the yield ratio of the corresponding correctly-identified components in the $B^\pm \rightarrow \phi K^\pm$ sample.

The fit procedure is validated on simulated data containing the expected proportion of signal and background events.

These studies, which take into account the different $\delta m$ distributions and the possible correlation between the fit observables, demonstrate the stability of the fit and show that the fit results are unbiased.

5. Measurement of the $B^\pm \rightarrow \phi K^\pm$ charge asymmetry

The charge asymmetry of the $B^\pm \rightarrow \phi K^\pm$ signal is determined from a fit to the $B^\pm \rightarrow \phi K^-$ and $B^+ \rightarrow \phi K^+$ candidates in the $\text{DLL}_{\pi} > -1$ region. These two samples are each divided into two subsamples according to whether the events were TOS or TIS at the hardware trigger stage. In the fit, each of the six components has therefore four yields. For the signal component, they are expressed as $N_{TOS}^s = N_{TOS} (1 - \delta_{\text{raw}, TOS}) / 2$ and $N_{TIS}^s = N_{TIS} (1 + \delta_{\text{raw}, TIS}) / 2$, where $N_{TOS}$ is the total yield and $\delta_{\text{raw}, k}$ is the raw yield asymmetry in subsample $k$ ($k = \text{TOS}, \text{TIS}$). The fit has a total of 34 free parameters: 10 mass shape parameters, 12 yields and 12 raw asymmetries.
Tables of the (a) $K^+K^-K^-$ and (b) $K^+K^-$ masses of the selected $B^-\to\phi K^-$ candidates, as well as of the (c) $K^+K^-K^+$ and (d) $K^+K^-$ masses of the selected $B^+\to\phi K^+$ candidates. The solid blue curves represent the result of the simultaneous fit described in the text, with the following components: $B^\pm\to\phi K^\pm$ signal (dotted red), nonresonant $B^\pm\to K^+K^-K^0$ background (dashed red), partially-reconstructed $b$-hadron background with (dotted blue) or without (dashed blue) a true $\phi$ meson, and combinatorial background with (dotted green) or without (dashed green) a true $\phi$ meson. Some of the components are barely visible because the corresponding yields are small. Normalized residuals are displayed below each histogram. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this Letter.)

| Table 1 |
|---|
| Raw charge asymmetries for the $B^\pm\to\phi K^\pm$ and $B^\pm\to J/\psi K^\pm$ decays, their difference $\Delta A_C$, and the fraction of $B^\pm\to\phi K^\pm$ signal events in each trigger subsample for $k=TOS,TIS$. All uncertainties are statistical only. |
| $\Delta A_C$ | TOS subsample | TIS subsample |
| $A_{raw,k}(B^\pm\to\phi K^\pm)$ | $+0.027\pm0.026$ | $-0.053\pm0.033$ |
| $A_{raw,k}(B^\pm\to J/\psi K^\pm)$ | $-0.024\pm0.008$ | $-0.008\pm0.005$ |
| $\Delta A_C$ | $+0.052\pm0.027$ | $-0.045\pm0.035$ |
| $N_k/(N_{TOS}+N_{TIS})$ | 66% | 34% |
| Weighted $\Delta A_C$ average | $+0.019\pm0.021$ |

Fig. 2 shows the projections of the fitting function superimposed on the $m_{KKK}$ and $m_{KK}$ distributions, shown separately for $B^-$ and $B^+$ candidates, but where TOS and TIS events are summed. The $m_{KKK}$ resolution measured from the fit is $\sigma_g=20.4\pm0.3$ MeV/c$^2$. The fitted raw asymmetries for the signal are shown in the first line of Table 1. They are statistically uncorrelated.

Each raw charge asymmetry is related to the $CP$ asymmetry through

$$A_{raw,k}(B^\pm\to\phi K^\pm) = A_{CP}(B^\pm\to\phi K^\pm) + A_{D,k}(B^\pm\to\phi K^\pm) + A_P,$$

where $A_{D,k}(B^\pm\to\phi K^\pm)$ is the detection charge asymmetry for the bachelor $K^\pm$ and $A_P$ is the production asymmetry of $B^\pm$ mesons. Eq. (8) and the corresponding equation for the $B^\pm\to J/\psi K^\pm$ reference channel hold because all involved asymmetries are small. Under the assumption that the detection asymmetry is the same for $B^\pm\to\phi K^\pm$ and $B^\pm\to J/\psi K^\pm$, which is correct in the limit where the bachelor $K^\pm$ has the same kinematic properties, the difference in charge asymmetries defined in Eq. (2) can be written as

$$\Delta A_{CP} = A_{raw,k}(B^\pm\to\phi K^\pm) - A_{raw,k}(B^\pm\to J/\psi K^\pm)$$

and should not depend on the trigger category $k$. The raw charge asymmetries of $B^\pm\to J/\psi K^\pm$ decays have been measured in a previous analysis [5]; they are subtracted from the $B^\pm\to\phi K^\pm$ raw asymmetries to obtain two independent measurements of $\Delta A_{CP}$. Since the two results agree within about two statistical standard deviations, the results are combined. The final $\Delta A_{CP}$ result is computed as a weighted average, with weights equal to the fractions $N_k/(N_{TOS}+N_{TIS})$ of signal events in the two trigger subamples. All inputs to the calculation are reported in Table 1. The separation between TIS and TOS events is needed because the detection asymmetry $A_{D,k}$ depends on the trigger category $k$ and the fraction of events in the two categories differs between the signal and reference channels.

Several systematic uncertainties are considered on the weighted $\Delta A_{CP}$ average, as summarized in Table 2. The contribution due to the mass shape modelling is obtained by repeating the fit (and the
calculation of Table 1) with the fixed parameter values of the Crystal Ball and ARGUS functions changed within their uncertainties, as determined from simulation and \( B^± \rightarrow \phi K^± \) data, respectively, or with an exponential (rather than linear) combinatorial background model. Possible residual effects from \( S \)-wave contributions not fully accounted for by the linear component are investigated by comparing the observed angular distribution of the \( B^± \rightarrow \phi K^± \) signal with the expectation for a peaking structure in the \( K^-K^+ \) mass due to a single \( P \)-wave state. Other \( P \)-wave components are neglected. If these \( S \)-wave contributions corresponded to an additional component included in the signal without charge asymmetry, a bias would appear on \( \Delta \mathcal{A}_{CP} \), which is taken as a systematic uncertainty.

The charge asymmetry in the trigger efficiency for kaons of the TOS subsample does not completely cancel in \( \Delta \mathcal{A}_{CP} \), because of the different number of kaons in the two decay modes considered. The difference between the values of \( \mathcal{A}_{raw,TOS}(B^± \rightarrow J/\psi K^±) \) computed with and without a charge-dependent correction for the kaon efficiency determined from calibration data is propagated as a systematic uncertainty on \( \Delta \mathcal{A}_{CP} \). Such an effect is absent for the TIS subsample. Another small contribution, due to the TOS events that would still be accepted by the hardware trigger level without considering the particles from the \( B^± \) candidate decay, has been included in the trigger systematic uncertainty. Due to differences in the kinematic selections of \( B^± \rightarrow J/\psi K^± \) and \( B^± \rightarrow J/\psi K^± \) decay modes, the assumption of Eq. (9) cannot be exact, and a further systematic uncertainty is assigned. The fit of the raw charge asymmetries of \( B^± \rightarrow J/\psi K^± \) is repeated with the same kinematic selection on the bachelor kaon as for \( B^± \rightarrow \phi K^± \), i.e. \( p > 10 \text{ GeV}/c \) and \( p_T > 2.5 \text{ GeV}/c \), and after reweighting its momentum distribution to that observed in the \( B^± \rightarrow \phi K^± \) decays. The resulting effect on \( \Delta \mathcal{A}_{CP} \) is taken as a systematic uncertainty.

Finally, we repeat the \( B^± \rightarrow \phi K^± \) analysis after requiring the bachelor kaon momentum to point in a fiducial solid angle avoiding detector edge effects, and assign the observed change in \( \Delta \mathcal{A}_{CP} \) as a systematic uncertainty due to the geometrical acceptance.

The final measurement is

\[
\Delta \mathcal{A}_{CP} = 0.019 \pm 0.021 \text{(stat)} \pm 0.007 \text{(syst)}.
\]

A recent update of the \( B^± \rightarrow J/\psi K^± \) charge asymmetry measurement by the D0 Collaboration [20] has not been included yet in the average of the Particle Data Group (PDG) [1]. Replacing the previous D0 result with the new one yields the world average \( \mathcal{A}_{CP}(B^± \rightarrow J/\psi K^±) = 0.003 \pm 0.006 \), where the uncertainty is scaled by a factor 1.8 according to the PDG averaging rules. Using this average, we obtain

\[
\mathcal{A}_{CP}(B^± \rightarrow \phi K^±) = 0.022 \pm 0.021 \text{(stat)} \pm 0.009 \text{(syst)},
\]

where the uncertainty on the \( B^± \rightarrow J/\psi K^± \) charge asymmetry is incorporated in the systematic uncertainty.

### 6. Search for \( B^± \rightarrow \phi \pi^± \) decays

The search for \( B^± \rightarrow \phi \pi^± \) decays is performed using a simultaneous fit to the \( B^± \rightarrow \phi \pi^± \) (\( \Delta \mathcal{L}_{K\pi} \geq -1 \)) and \( B^± \rightarrow \phi K^± \) (\( \Delta \mathcal{L}_{K\pi} \geq -1 \)) candidates, dividing the \( B^± \rightarrow \phi \pi^± \) candidates in four subsamples according to their \( \delta m \) values, each with its set of eight yields. The fit has a total of 52 free parameters: 15 mass shape parameters, 36 yields, and the ratio of the total \( B^± \rightarrow \phi \pi^± \) yield to the total \( B^± \rightarrow \phi K^± \) yield.

Fig. 3 shows the projections of the fitted function superimposed on the observed mass distributions of the \( B^± \rightarrow \phi \pi^± \) candidates. The total \( B^± \rightarrow \phi \pi^± \) signal yield is found to be 19 ± 19, while the total \( B^± \rightarrow \phi K^± \) yield is \( (3486 \pm 76) + (280 \pm 25) \) summing the samples of \( B^± \rightarrow \phi K^± \) and \( B^± \rightarrow \phi \pi^± \) candidates. The fitted yield ratio is

\[
\frac{N(B^± \rightarrow \phi \pi^±)}{N(B^± \rightarrow \phi K^±)} = (5.1^{+5.3}_{-5.0}(\text{stat}) \pm 2.1(\text{syst})) \times 10^{-3},
\]

where the systematic uncertainty is the quadratic sum of contributions due to the modelling of the mass shapes (\( \pm 2.1 \times 10^{-3} \)), the fit procedure (\( \pm 0.2 \times 10^{-3} \)), and interference effects between the \( \phi \) resonance and a \( K^-K^+ \) pair in an \( S \)-wave state (\( \pm 0.4 \times 10^{-3} \)). The first contribution is obtained by repeating the fit with the parameter values of the Crystal Ball and ARGUS functions changed within their uncertainties, or with an exponential (rather than linear) combinatorial background model. The dominant effect is due to the 8% uncertainty on the ratio \( \rho \) of the \( B^± \rightarrow \phi K^± \) mass resolutions in the two \( \Delta \mathcal{L}_{K\pi} \) regions. Simulation studies show that the fit procedure is unbiased, and the statistical precision of this check is assigned as a systematic uncertainty.

The measurement of the branching fraction ratio is obtained as the ratio between Eq. (12) and Eq. (3):

\[
\frac{B(B^± \rightarrow \phi \pi^±)}{B(B^± \rightarrow \phi K^±)} = (6.6^{+6.9}_{-6.6}(\text{stat}) \pm 2.8(\text{syst})) \times 10^{-3}.
\]

Since the result is not significantly different from zero, we also quote upper limits from the integral of the likelihood function of this ratio, considering only the physical (non-negative) region. Including systematic uncertainties we obtain \( B(B^± \rightarrow \phi \pi^±)/B(B^± \rightarrow \phi K^±) < 0.018(0.020) \) at 90% (95%) CL. Using the current world average \( B(B^± \rightarrow \phi \pi^±) = (8.8^{+0.7}_{-0.6}) \times 10^{-6} \) [1], we finally obtain

\[
B(B^± \rightarrow \phi \pi^±) = (5.8^{+6.1}_{-5.8} \pm 2.5) \times 10^{-8} < 1.5(1.8) \times 10^{-7} \text{ at 90% (95%) CL.}
\]

### 7. Conclusions

The difference in charge asymmetries between the \( B^± \rightarrow \phi K^± \) and \( B^± \rightarrow J/\psi K^± \) decay modes is measured in a sample of pp collisions at 7 TeV centre-of-mass energy, corresponding to an integrated luminosity of 1.0 fb\(^{-1}\) collected with the LHCb detector. Using the known value of the \( B^± \rightarrow J/\psi K^± \) asymmetry, the \( CP \)-violating charge asymmetry of \( B^± \rightarrow \phi K^± \) decays is determined to be \( \mathcal{A}_{CP}(B^± \rightarrow \phi K^±) = 0.022 \pm 0.021 \text{(stat)} \pm 0.009 \text{(syst)} \). This result is almost a factor two more precise than the current world average [1]. It is consistent with both the absence of \( CP \) violation and the Standard Model prediction.

A search for \( B^± \rightarrow \phi \pi^± \) decays is also performed. No significant signal is found. Using the known branching fraction of the \( B^± \rightarrow \phi K^± \) normalization channel, an upper limit of \( B(B^± \rightarrow \phi \pi^±) < 1.5(1.8) \times 10^{-7} \) is set at 90% (95%) confidence level. This improves on the previous best upper limit [19], while reaching the upper end of the Standard Model predictions.

### Acknowledgements

We express our gratitude to our colleagues in the CERN accelerator departments for the excellent performance of the LHC.

### Table 2

| Source                              | Uncertainty  |
|-------------------------------------|--------------|
| Mass shape modelling                | 0.003        |
| Possible \( S \)-wave contribution  | 0.002        |
| Trigger                             | 0.004        |
| Bachelor kaon kinematic properties  | 0.005        |
| Geometric acceptance                | 0.002        |
| Quadratic sum                       | 0.007        |
Fig. 3. Distributions of the (a, c) \(K^+K^-\pi^\pm\) and (b, d) \(K^+K^-\) masses of the selected \(B^\pm\to\phi\pi^\pm\) candidates, shown both with linear and logarithmic scales. The solid blue curves represent the result of the simultaneous fit described in the text, with the following components: \(B^\pm\to\phi\pi^\pm\) signal (dotted black), nonresonant \(B^\pm\to\phi K^+ K^-\) background (dashed black), \(B^\pm\to\phi K^+\) signal (dotted red), nonresonant \(B^\pm\to\phi K^+ K^-\) background (dashed red), partially-reconstructed \(b\)-hadron background with (dotted blue) or without (dashed blue) a true \(\phi\) meson, and combinatorial background with (dotted green) or without (dashed green) a true \(\phi\) meson. Normalized residuals are displayed below the histograms. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this letter.)

We thank the technical and administrative staff at the LHCb institutes. We acknowledge support from CERN and from the national agencies: CAPES, CNPq, FAPERJ and FINEP (Brazil); NSFC (China); CNRS/IN2P3 and Region Auvergne (France); BMBF, DFG, HGF and MPG (Germany); SFI (Ireland); FOM and NWO (The Netherlands); KRF and KOSEF (Korea); INP (Russia); INFN (Italy); FOI and NWO (The Netherlands); SCSR (Poland); MEN/IFA (Romania); MinEES, Rosatom, RFBR and NRC “Kurchatov Institute” (Russia); MinECo, XuntaGal and GENCAT (Spain); SNF and SER (Switzerland); NAS Ukraine (Ukraine); STFC (United Kingdom); NSF (USA). We also acknowledge the support received from the ERC under FP7. The Tier1 computing centres are supported by IN2P3 (France), KIT and BMBF (Germany), INFN (Italy), NWO and SURF (The Netherlands), PIC (Spain), GridPP (United Kingdom). We are thankful for the computing resources put at our disposal by Yandex LLC (Russia), as well as to the communities behind the multiple open source software packages that we depend on.

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