Parameter estimation of atherosclerotic tissue optical properties from three-dimensional intravascular optical coherence tomography

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Abstract. We developed robust, three-dimensional methods, as opposed to traditional A-line analysis, for estimating the optical properties of calcified, fibrotic, and lipid atherosclerotic plaques from in vivo coronary artery intravascular optical coherence tomography clinical pullbacks. We estimated attenuation $\mu_t$ and backscattered intensity $I_b$ from small volumes of interest annotated by experts in 35 pullbacks. Some results were as follows: noise reduction filtering was desirable, parallel line (PL) methods outperformed individual line methods, root mean square error was the best goodness-of-fit, and $\alpha$-trimmed PL ($\alpha$-T-PL) was the best overall method. Estimates of $\mu_t$ were calcified ($3.84 \pm 0.95 \text{ mm}^{-1}$), fibrotic ($2.15 \pm 1.08 \text{ mm}^{-1}$), and lipid ($9.99 \pm 2.37 \text{ mm}^{-1}$), similar to those in the literature, and tissue classification from optical properties alone was promising.© The Authors. Published by SPIE under a Creative Commons Attribution 3.0 Unported License. Distribution or reproduction of this work in whole or in part requires full attribution of the original publication, including its DOI: [10.1117/1.JMI.2.1.016001]

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1 Introduction

Intravascular optical coherence tomography (IVOCT) provides unique high-contrast microscopic resolution imaging of the vasculature. With regard to atherosclerotic plaques, IVOCT has demonstrated an ability to differentiate lipid, calcium, and fibrous tissue and to quantify microscopic features such as macrophage content. We have previously reported on IVOCT image analysis relating to segmentation, quantification, and classification of various plaque features and confuse IVOCT image quality is affected by any residual blood, but this is not a major concern with current OCT images in vascular and other tissues using a variety of experimental and theoretical methods. Most use a single-scattering model. We will review reports that measured attenuation and backscattering coefficients in vascular tissues first. Xu et al. used a noncatheter-based approach by imaging transverse, fixed tissue sections of coronary arteries; averaged 400 A-lines over time; applied a single-scattering light model; and performed least squares fitting of log transformed, average A-lines to a linear equation. It was concluded that the calcified and fibrotic plaques had a much lower optical attenuation coefficient, $\mu_t$, than lipid plaques, and that lipid and fibrotic plaques had a much higher backscattering coefficient, $\mu_b$, than calcified plaques (lipid: $\mu_b = 28.1 \pm 8.9 \text{ mm}^{-1}$, $\mu_t = 13.7 \pm 4.5 \text{ mm}^{-1}$, calcified: $\mu_b = 4.9 \pm 1.5 \text{ mm}^{-1}$, $\mu_t = 5.7 \pm 1.4 \text{ mm}^{-1}$, and fibrotic: $\mu_b = 18.4 \pm 6.4 \text{ mm}^{-1}$, $\mu_t = 6.4 \pm 1.2 \text{ mm}^{-1}$). Using a catheter-based system and a stationary acquisition without pullback, van Soest et al. measured $\mu_t$ in both in vivo and
ex vivo specimens. They corrected for the nonideal imaging system; averaged 15 to 20 A-lines in time; fitted a linear model to log transformed data; and applied an elegant algorithm to determine regions in one dimension corresponding to a single, homogenous tissue type. van Soest et al. argued that \( \mu_s \) cannot be estimated accurately along with \( \mu_t \) using a single magnitude OCT value alone at each point and reported only \( \mu_t \) for calcified (2 to 5 mm\(^{-1}\)), fibrotic (2 to 5 mm\(^{-1}\)), and lipid (>10 mm\(^{-1}\)), yielding trends similar to values reported by Xu et al.\(^{29}\) Levitz et al.\(^{31}\) applied a multiple scattering model to OCT images of phantoms and ex vivo aortas and estimated scattering coefficients and anisotropy factors. In other studies, OCT data from both phantoms and ex vivo arterial samples were fit to single and multiple scattering models.\(^{32,33}\) Since temporal averaging of frames from a stationary acquisition is undesirable in the clinical setting, frequency domain multiplexing with improvement as compared with simple linear filtering has been proposed to reduce speckle in single A-lines for optical property measurement.\(^{34}\) As reviewed in Sec. 5, there is variability in reported \( \mu_s \) values between research groups due to methodological differences including parameter estimation approaches.

Optical properties have also been estimated in other tissues using OCT. Yang et al.\(^{35}\) determined the optical scattering coefficient, \( \mu_s \), from unfixed normal and malignant, ex vivo ovarian tissues. They found that the absorption coefficient, \( \mu_a \), for ovarian tissue is small (<0.006 mm\(^{-1}\)) and that \( \mu_s \) was a good approximation to \( \mu_a \). Knu et al.\(^{26}\) determined the optical parameters from OCT images of pig and human skin using a multiple scattering model. Lee et al.\(^{36}\) have studied the performance of a single-scattering model. Lee et al.\(^{36}\) have studied the performance of a single-scattering model.

A goal is to fully automate tissue characterization in 3-D IV OCT clinical pullbacks. Some recent reports use machine learning for plaque classification from both preclinical and clinical IV OCT data.\(^{37,38}\) Ughi et al.\(^{38}\) used \( \mu_t \) estimates from a layer model applied to single A-lines and two-dimensional (2-D) texture and geometric measures as features for classification. Athanasiou et al.\(^{37}\) used 2-D texture and intensity features alone and assumed “islands” of calcified tissue surrounded by other tissue types, which is not necessarily true in many image frames. These reports are encouraging and show that improved 3-D estimation of optical properties could improve the classification.

The rationale for our research plan is as follows. Although it is clear that the optical properties of plaques, such as the attenuation coefficients, will be useful discriminatory features for automated tissue classification, extracting optical properties from clinical IV OCT data remains a challenge. Stationary acquisitions\(^{25,30}\) are untenable, as they will require an additional blood clearing operation to sample a single location. Estimation from single, noisy A-lines gives large estimation variance. Hence, our solution is to estimate optical properties from small 3-D volumes of pullback image data and to use advanced parameter estimation approaches which are robust against noise outliers. In addition, we use in vivo clinical data rather than image data from ex vivo samples as is typically used. This avoids typical limitations of ex vivo imaging including potential tissue degradation, no mean and/or pulsating pressure, no cardiac motion, unrealistic temperatures, no blood artifacts, and a straight path pullback rather than actual 3-D coronary geometry. Moreover, in the event of spatially inaccurate, sparse histological sampling, one can make inappropriate “ground truth” determinations using ex vivo data. Instead we use ground truth volumes of interest (VOIs) identified by trained analysts using well-established criteria. Although independent histological verification is desirable, there is no way to obtain it on in vivo clinical data. Moreover, our approach is quite appropriate for optimizing the 3-D parameter estimation methods in this report. Methods should be equally applicable to 3-D cancer imaging.

In this report, we correct the nonideal characteristic of OCT imaging systems, use noise reduction filtering, estimate optical parameters from small VOIs rather than single A-lines, reject outliers, identify goodness-of-fit measures suitable for determining the quality of optical property estimates, and determine how well optical properties alone can be used to classify plaque types. Our basic paradigm is to compare estimation results across 311 manually annotated VOIs.

## 2 Experimental Methods and Catheter Correction

Images used in this study were selected from the database available at the Cardiovascular Imaging Core Laboratory of the University Hospitals Case Medical Center (Cleveland, Ohio), called the Core Lab. These images were collected on the C7-XR swept-source OCT system (St. Jude Medical Inc., Westford, Massachusetts). It has a swept laser source with a 1310-nm center wavelength, 110-nm wavelength range, 50-kHz sweep rate, 20-mW output power, and ~12-mm coherence length. The pullback speed was 20 mm/s and the pullback length was 54 mm. A typical pullback consisted of 271 image frames spaced ~200 \( \mu \)m apart. The test dataset consisted of 35 IV OCT pullbacks of the left anterior descending and the left circumflex coronary arteries and was chosen to be representative of typical OCT scans obtained from patients prior to stent implantation.

To more accurately estimate \( \mu_t \), we need to account for certain characteristics of the IV OCT imaging system. We used methods similar to those of van Soest et al.\(^{40}\) The imaging system response in the presence of tissue attenuation \( \mu_t \) is given below:\(^{30}\)

\[
I(r) = I_0 T(r) S(r) \exp(-\mu_t r) + I_{\text{off}}. \tag{1}
\]

with

\[
T(r) = \left( \frac{r-z_0}{z_R} \right)^2 + 1 \right)^{-1/2}, \tag{2}
\]

\[
S(r) = \exp\left( -\frac{r-z_C}{z_W} \right)^2, \tag{3}
\]

where \( r \) is the depth, \( I \) is the detected intensity, \( I_0 \) is the initial intensity, \( I_{\text{off}} \) is the detected intensity at a depth of \( r = 0 \), \( \mu_t \) is the attenuation coefficient, \( T(r) \) is the confocal function with \( z_0 \), the position of the beam waist and with \( z_R \), the Rayleigh length, and \( S(r) \) accounts for the spectral coherence of the source in Fourier-domain OCT with parameters \( z_W \) (representing the half-width of the intensity roll off) and \( z_C \) (representing the center of the scan).
Intact catheters without a guide wire were inserted into a bottle containing water or low concentration intralipid solution. The catheter was firmly held in place using a vice-grip on the catheter outside the bottle. The water image was used to estimate background intensity. A low concentration 1:128 intralipid (Sigma Aldrich, 20%, emulsion) diluted in water provided an image of scatterers without significant attenuation. Stationary image sequences of 121 image frames and pullback sequences of 271 image frames were obtained. About 100 IV OCT magnitude images were averaged. From the average frame, we averaged 500 A-lines to obtain a very low noise A-line.

In intralipid images, we assumed $\mu_t$ to be low, eliminating the tissue attenuation term $\exp(-\mu_r r)$. $I_{\text{off}}$ was estimated from the water images. $z_c$ and $z_w$ were obtained from the interferometer setting and the specifications of the light source, respectively. With these parameters fixed, $I_0$, $z_0$, $a$, and $r_0$ were estimated by fitting Eq. (1) to average A-line data using nonlinear least squares with the Nelder–Mead simplex optimization. A-line data were truncated to exclude bright reflection from the catheter sheath. Model fits were compared over pullbacks, catheters, and acquisition modes (stationary versus pullback). Similar fits were obtained in each case with less than 3% variation in parameters. Clinical images were corrected using Eq. (1). We subtracted $I_{\text{off}}$, the baseline intensity, and divided A-line intensities by the term $I_0 \cdot T(r) \cdot S(r)$.

3 Image Analysis

3.1 Volumes of Interest

We developed specialized software in MATLAB for obtaining user-defined VOIs and for evaluating their optical properties. In the software, pullbacks were loaded and image frames were presented to the expert, an IV OCT image analyst, in both $(x, y)$ and $(r, \theta)$ views. Image data came from a manually analyzed Core Lab study aimed at classifying plaque types and plaque burden prior to stent implantation. The study classified quadrants of IV OCT images as either fibrous, lipid, calcium, or normal. Core Lab analysts were well trained in interpreting OCT image data. For our study, the analyst determined start and stop image frames for a homogeneous VOI. Then, in the $(r, \theta)$ view, the analyst segmented the VOI using freehand brush strokes and applied a plaque-type label (fibrous, lipid, or calcified). All segmentations and labels for VOIs were saved in a convenient data structure for easy retrieval and analysis. Standard criteria were used by analysts to identify the various plaque types in pullback image frames. Fibrous plaques were characterized by homogeneous, signal-rich regions; calcified regions by signal-poor regions with sharp borders; and lipid plaques by signal-poor regions with diffuse borders. In this study, we used 311 VOIs from 35 pullbacks. The VOIs were of various sizes and shapes. Most consisted of 2 to 5 image frames, 50 to 200 A-lines, and 20 to 50 sample points in each A-line.

3.2 Parameter Estimation of Tissue Optical Properties

Each VOI was processed as follows. We applied 2-D noise reduction filtering to linear data using a variety of filters [average filter (AF), median filter (MF), and Lee speckle reduction filter (LF)] with parameters listed later. To avoid any “edge effects” during filtering, we applied 2-D filtering to entire image frames and subsequently used the stored spatial coordinates of each VOI to extract a “filtered” VOI. Any A-line with fewer than five samples (points) was removed from consideration. Rearranging and taking the natural logarithm of Eq. (1), we get the equation below:

$$\ln \left\{ \frac{[I(r) - I_{\text{off}}(r)]}{[T(r; z_0, z_R) \cdot S(r)]} \right\} = \ln(I_0) - \mu_r r. \quad (4)$$

In the event that the left-side term within square brackets was ≤0, we set its value to +1. Equation (4) reduces to fitting a straight line to the data. Parameter estimation methods included individual line (IL) fits and parallel line (PL) fits to A-lines. In IL fitting, a slope and intercept are fit to each A-line in a collection of adjacent A-lines. In PL fitting, we fit one slope and multiple intercepts to the collection as is rationalized next. Assuming locally homogeneous tissue within a VOI, there should be a single characteristic $\mu_t$ value and a single slope. Intercepts depend upon distance from the catheter, the angle of incidence with the lumen, depth in tissue, and so on, which are observations consistent with the PL approach. Moreover, a PLs’ model has many fewer parameters making it less sensitive to noise. In addition, we have also employed methods that perform statistical analysis to reject data outliers for which we use the term “robust.” The methods were:

- **IL, individual A-lines**: Each corrected A-line was fit to Eq. (4) yielding a set of $\mu_t$ and $I_0$ values. Extreme outliers, i.e., lines with negative $\mu_t$, were removed. Means of $\mu_t$ and $I_0$ were reported. Standard errors (SEs) were computed from $SE = SD/\sqrt{n}$, where SD is the standard deviation and $n$ is the number of A-lines processed.

- **$\alpha$-T-IL, individual A-lines with a trimming**: In this robust parameter estimation approach, we determined $\mu_t$ and $I_0$ for each A-line, removed extreme outliers, and rank ordered results. A predetermined percentage, $\alpha$, of $\mu_t$’s (and corresponding $I_0$’s) from the top and bottom of the distribution was removed, and new mean $\mu_t$ and $I_0$ values were obtained. SEs were computed using the same strategy as above.

- **IT-IL, individual A-lines with iterative trimming**: In this robust parameter estimation approach, we determined $\mu_t$ and $I_0$ for each A-line, removed extreme outliers, and computed a new mean $\mu_t$ and $I_0$. We then iteratively removed A-lines with $\mu_t$’s outside mean ± 2 (SD), with empirically determined $n = 3$ iterations. Finally, a mean $\mu_t$ and $I_0$ were computed from the remaining A-lines and reported. SEs were computed as above.

- **PL, Parallel line fit to A-lines**: We determined a $\mu_t$ and $I_0$ for each A-line using IL fits and removed extreme outliers. On the remaining A-lines, a PL model with a single slope and multiple intercepts was estimated, giving a single $\mu_t$ and multiple $I_0$’s. SEs were computed from the MATLAB toolbox function aoctool.

- **$\alpha$-T-PL, Parallel lines with a trimming**: In this robust approach, we determined a $\mu_t$ and $I_0$ for each A-line using IL fits, removed extreme outliers, and rank ordered results. A predetermined percentage, $\alpha$, of $\mu_t$’s (and corresponding $I_0$’s) from the top and bottom of the distribution was removed. A PL model was
applied to the remaining A-lines. Parameter uncertainty errors were computed as above.

**IT-PL, Parallel lines with iterative trimming:** In this robust approach, we determined a \( \mu_t \) and \( I_0 \) for each A-line using IL fits, removed extreme outliers, and computed a new mean \( \mu_t \) and \( I_0 \). We then iteratively removed A-lines with \( \mu_t \)’s outside the mean \( \pm 2(\text{SD}) \) with an empirically determined \( n = 3 \) iterations. A PL model was applied to the remaining A-lines. Parameter uncertainty errors were computed as above.

**NIL-PL-TM, Individual lines followed by parallel lines followed by noniterative trimming:** In this robust approach, we determined a \( \mu_t \) and \( I_0 \) for each A-line using IL fits, removed extreme outliers, and applied a PL fit to obtain a single-slope \( \mu_{PL} \) and a standard deviation \( SD_{PL} \). Next, we kept only those A-lines with individual \( \mu_t \)’s within \( \mu_{PL} \pm 2(\text{SD}_{PL}) \). We then computed mean \( \mu_t \) and \( I_0 \) and reported values. SEs were computed using the strategy for IL.

**IL-PL-TM, Individual lines followed by parallel lines followed by iterative trimming:** In this robust approach, we determined \( \mu_t \) and \( I_0 \) for each A-line using IL fits and removed extreme outliers. We applied a PL model to obtain a single-slope \( \mu_{PL} \) and a standard deviation \( SD_{PL} \). Next, we kept only those A-lines with individual \( \mu_t \)’s within \( \mu_{PL} \pm 2(\text{SD}_{PL}) \). We then computed mean \( \mu_t \) and \( I_0 \) from the IL fits. SEs were computed using the strategy for IL.

### 3.3 Data Analysis

For each VOI, we obtained \( \mu_t \) and \( I_0 \) estimates for each combination of filtering (three methods) and parameter estimation (eight methods). Goodness-of-fit measures included coefficient of variation (CV) given by the ratio of the parameter uncertainty to the point estimate, the root mean square error (RMSE), and adjusted \( R^2 \), calculated as described in Ref. 40. For good filtering and estimation methods, we want: (1) small parameter uncertainty intervals, (2) small spread of point estimates across many VOIs of a particular tissue type, (3) superior goodness-of-fit values (high adjusted \( R^2 \), low RMSE, and low CV), and (4) high sensitivity/specificity from parameter estimates using a supervised classifier.

### 3.4 Processing Parameters

We optimized the processing parameters in preliminary experiments. The size of the filter window \((7 \times 7)\) and other parameters was tuned by examining their role on image appearance as well as \( \mu_t \) estimates. It should be noted that a filter kernel of length 7 is approximately the same size as the 35 \( \mu m \) axial point spread function of our system. We used a \( 7 \times 7 \) window for the LF, AF, and MF. Since VOIs were of irregular shape, we obtained some short A-line segments which were omitted if they contained fewer than five samples. To avoid fitting the baseline noise floor, we ended consideration of A-line samples along \( r \) when there was a run of nine samples below the baseline value of six in the original linear data. This occurred in less than 1% of A-lines as experts did not mark VOIs at large depths in the tissue. For robust estimation with a trimming, we experimentally determined an optimal value of \( \alpha = 10\% \). For iterative estimation methods, we experimentally determined that three iterations and two SDs gave good results. More details about optimization experiments are in Sec. 4.

In an exploratory classification experiment, we used three features \((\mu_t, I, I_0)\), and a support vector machine (SVM) classifier with a linear kernel, fivefold cross validation, and feature normalization. We used one-against-all to identify three tissue

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**Fig. 1** Appearance of atherosclerotic tissue types in IVOCT images. They are: (a) fibrous, (b) lipid, (c) calcium, and (d) normal (media). The latter includes a zoomed inset to show the typical layered appearance. In (e) and (f), a sample IVOCT image frame is shown in the \((x, y)\) (anatomical) and \((r, \theta)\) (polar) views, respectively. A calcified region is identified in red in both frames.
types. Parameter settings of the classifier were determined from preliminary optimization experiments with a subset of VOIs. We weighted samples in inverse proportion to their prevalence. Performance results were averaged across the five folds.

4 Results

Example IVOCT images in Figs. 1(a)–1(d) show calcified, fibrotic, lipid, and normal (media) regions in the \((x, y)\) view. Figures 1(e) and 1(f) show a sample IVOCT image frame from a clinical pullback in both \((x, y)\) (anatomical) and \((r, \theta)\) (polar) views, with a calcified region identified in red. The VOIs were marked on \((r, \theta)\) view because all subsequent processing were done on \((r, \theta)\) image data. The VOIs were mapped to \((x, y)\) for presentation (Fig. 2). We have observed that, in general, the tissue types in a region of interest do not change much across successive frames, i.e., they have a high correlation, justifying the use of volumetric analysis in our study (Fig. 2).

We obtained images of intralipid and water and fitted the data to the system model. Average A-lines from a stationary acquisition are shown in Fig. 3. We ignored the very small upward trend in water and used an average value for \(I_{off}\). Water images were similar across the three tested catheters, and \(I_{off}\) values were close to baseline values at large \(r\) in clinical images. Using the average A-line from dilute intralipid images, Eq. (1) was fit to data over the “imaging range” from 1 to 2.5 mm. As described previously, values for \(I_0\), \(z_0\), and \(z_R\) were estimated using a least squares fit [Fig. 3(b)] and other parameters were obtained from system specifications. Parameters for the typical catheter in Fig. 3 were: \(I_0 = 155\), \(z_0 = 1.06\) mm, \(z_R = 0.59\) mm, \(I_{off} = 6.39\), \(z_C = 0\) mm, and \(z_W = 12\) mm.

We determined the sensitivity of \(\mu_t\) estimates to the correction model parameter estimates. Table 1 shows the result for representative VOIs using PLs to estimate \(\mu_t\). Values of \(\mu_t\) changed by only 3% to 7% with and without catheter correction. To study the potential effect of variation between catheters, we perturbed catheter parameters over a \(\pm 5\%\) range (a variation much larger than observed) and determined the effect on \(\mu_t\). In general, different catheter correction parameters had a relatively minor effect (typically \(<3\%) on \(\mu_t\), smaller than the uncertainty due to noise (see Sec. 4). Varying \(z_0\) had a bigger effect than varying \(z_R\).

Preprocessing methods were systematically tuned. Individual A-lines with speckle were quite noisy and were visually evident only after filtering trends. Using IL parameter estimation, noise reduction filters substantially reduced SE uncertainties of \(\mu_t\) estimates [Fig. 4(a)]. SE was reduced from 0.8442 [no filtering (NF)] to 0.5371 using AF, 0.446 using MF, and 0.1923 using LF. Therefore, LF was deemed the best filtering approach. Small variations in point estimates were obtained, but effects were

![Fig. 2](https://example.com/fig2.png)

**Fig. 2** Marking of VOIs in images across frames. Columns contain three successive image frames for (1a–1c) calcium, (2a–2c) lipid, and (3a–3c) fibrous, corresponding to a single VOI. Because tissue types are preserved across a few image frames with 200 \(\mu\)m spacing, we can process A-lines within VOIs. In practice, such multiple VOIs would be obtained from a single homogenous region (not shown).
inconsistent across VOIs, reducing the concern of potential bias. Effects of noise reduction were less dramatic when using other parameter estimation approaches, but trends were similar. Since we want estimates to help distinguish one tissue type from another, we analyzed the effect of filtering on the spread of estimates for a single tissue type across many VOIs. For calcium, LF reduced the spread of estimates by about 13% [Fig. 4(b)]. Similar results were obtained across other tissue types.

To optimize $\alpha$ in noniterative trimming, we varied $\alpha$ from 0% to 40% in steps of 5%, and at each step, we computed $\mu_t$ and the resulting RMSE for each VOI in a set of 84 VOIs drawn from all three plaque types. Figure 5 shows the average RMSE across VOIs plotted against $\alpha$. The optimum RMSE was $\alpha = \alpha_0 = 10\%$, and this was used in subsequent experiments. Similarly, we optimized $k$ in iterative trimming, which preserved A-lines with $\mu_t$s in the range (mean ± k · std). We estimated $\mu_t$ and RMSE with $k = 1, 2, \text{or} 3$ and obtained an average RMSE versus $k$ curve. The optimal $k = 2$ was used in subsequent experiments (not shown).

### Table 1

| Tissue type | No correction | Correction w/ Cath 5 | $z_0 = 0.984$ mm −5%/ + 5% | $z_R = 0.628$ mm −5%/ + 5% |
|-------------|---------------|---------------------|-----------------------------|-----------------------------|
| Calcium     | 2.54          | 2.35                | 2.34 (0.43%)/2.37 (0.85%)   | 2.36 (0.43%)/2.35 (0%)      |
| Fibrotic    | 2.08          | 2.00                | 2.06 (3%)/1.91 (4.5%)       | 2.00 (0%)/1.99 (0.5%)       |
| Lipid       | 5.50          | 5.14                | 5.13 (0.19%)/5.16 (0.39%)   | 5.16 (0.39%)/5.13 (0.19%)   |

Note: All numbers in table refer to the $\mu_t$ estimate in mm$^{-1}$.
We next compared the parameter estimation approaches. Figure 6 illustrates IL and PL. In this calcified VOI, PL gave a reduced parameter uncertainty (which results in a more robust and accurate estimate) as compared with IL (see legend). Using processing parameters from the above paragraph and LF, we examined the effects from the eight parameter estimation approaches. For a typical calcium VOI, $\alpha$-T-PL and PL gave smaller parameter uncertainty and SEs than other techniques (Fig. 7). There were small changes in point estimates, but across VOIs, there were no obvious trends. Over 111 fibrotic VOIs, the distribution of $\mu_t$ as a function of estimation methods is shown in Fig. 8(a) without censoring and Fig. 8(b) with censoring. Censoring was done to remove VOIs having bad fits, i.e., RMSE > 6. With censoring on RMSE, the number of outliers...
Fig. 7 Comparison of parameter estimation methods. A typical calcium VOI containing 62 A-lines was analyzed following LF. The following results were obtained (mean ± std. error of μ_t): (1) IL: 3.99 ± 0.27 (8 lines removed), (2) α-T-IL: 4.11 ± 0.18 (24 lines removed), (3) IT-IL: 4.03 ± 0.24 (14 lines removed), (4) PL: 3.81 ± 0.08 (8 lines removed), (5) α-T-PL: 4.17 ± 0.08 (24 lines removed), (6) IT-PL: 3.93 ± 0.09 (14 lines removed), (7) NIL-PL-TM: 3.78 ± 0.11 (38 lines removed), and (8) IL-PL-TM: 3.78 ± 0.11 (39 lines removed). α-T-PL and PL methods gave the smallest estimated uncertainty.

Fig. 8 Box whisker plot of μ_t as a function of estimation methods for (a) 111 fibrotic VOIs, and (b) a censored subset of 79 VOIs obtained by applying an RMSE threshold of 6. The red bar is the median, the edges of box are 25th and 75th percentiles, and the whiskers represent the most extreme points that are not outliers. Outliers are denoted with red +’s. The RMSE censoring greatly reduced the number of very large outliers and spread of μ_t estimates. With censoring, rank ordering on standard deviation across VOIs is α-T-PL < PL < IT-IL < α-T-IL < IL-PL-TM < IT-PL < IL-PL-TM < IL. The (mean ± std) of μ_t for methods is: IL (2.55 ± 1.16), α-T-IL (2.26 ± 1.10), IT-IL (2.35 ± 1.10), PL (2.14 ± 1.09), α-T-PL (2.18 ± 1.09), IT-PL (2.18 ± 1.11), NIL-PL-TM (2.06 ± 1.10), and IL-PL-TM (2.03 ± 1.13).
in $\mu_t$ was greatly reduced. Since censoring tended to remove VOIs having very large $\mu_t$ estimates, means were reduced with censoring. Also, the error bars were smaller after censoring as compared with before censoring, which meant that the $\mu_t$ estimates were more robust after censoring.

Since we are ultimately interested in automated processing, we analyzed the role of the size of the region of support on $\mu_t$ estimates. Figure 9 shows a scatter plot of numbers of A-lines in VOIs versus SE of $\mu_t$. In general, lower SEs were obtained for VOIs containing more A-lines. A large percentage (>80%) of VOIs had 50 or more A-lines in them. This suggests that the experts identified many homogeneous regions with >50 A-lines and average length of 35 samples. The VOIs having at least 50 A-lines resulted in an SE of typically <5% of the $\mu_t$ estimate.

We are especially interested in goodness-of-fit measures because they could become features in an automated machine learning approach to classify plaque types. Adjusted $R^2$ (Ref. 40) is a good method for comparing fits of models with different numbers of parameters [Fig. 10(a)]. Methods $\alpha$-T-PL, PL, and IT-PL had higher adjusted $R^2$ than other methods, indicating the appropriateness of PLs, a general observation across VOIs. We observed improvements with PLs because the number of free parameters was reduced from $2M$ to $M + 1$, where $M$ was the number of A-lines. Although the adjusted $R^2$ is a good method to compare model order, its dependence on slope does not allow comparisons across VOIs. For fibrous VOIs, RMSE and CV histograms were plotted [Figs. 10(b) and 10(c)].

More than 90% of VOIs had RMSE < 12. The RMSE was deemed the most appropriate goodness-of-fit for censoring VOIs. When VOIs with large RMSEs were omitted, the variability of $\mu_t$ estimates was reduced (Fig. 8) and classification (Table 3) improved.

To evaluate the usefulness of optical properties as features in an automatic classifier for atherosclerotic plaque tissue types, we used three features ($\mu_t, \langle I \rangle, I_{0}$), where $\langle I \rangle$ was the mean intensity in the VOI. Intensity features are related to the back-scattering characteristics of the tissue within the VOI as well as any attenuation prior to the VOI, features which should aid prediction of class membership. We used supervised classification, SVM,\textsuperscript{41} fivefold cross validation, and one against all for each of the three classes (Table 3). Data were processed without and with RMSE-based censoring, where VOIs with RMSE > 12 were excluded. Classification improved with censoring [compare Tables 3(a) and 3(b)]. (The RMSE threshold is different from that used in Fig. 8 because we wanted to be uniform across all three tissue classes.) Figure 11(a) shows a clear separation of classes in 3-D feature space following VOI censoring. Features ($\mu_t, \langle I \rangle$), the two best features, also demonstrated good separation in Fig. 11(b).

With all analyses considered, we determined that the PLs and $\alpha$ trimming were both useful, with PL and $\alpha$-T-PL producing numerically close $\mu_t$ estimates. In general, we recommend $\alpha$-T-PL, LF, and possible censoring on RMSE value as best choices. Using these choices, we obtained the following values of $\mu_t$: calcified ($3.84 \pm 0.95$ mm$^{-1}$), fibrotic ($2.15 \pm 1.08$ mm$^{-1}$), and lipid ($9.99 \pm 2.37$ mm$^{-1}$). Computational estimation of $\mu_t$ allowed us to distinguish between lipid plaques and calcium

![Fig. 9 Effect of number of A-lines on $\mu_t$ estimates. SE of $\mu_t$ estimates tends to reduce with VOIs having more A-lines. Processing included LF, $\alpha$-T-PL, no censoring. Tissue types are color coded. The mean number of A-lines was 150 and 80% of homogenous regions have $\geq 50$ A-lines. The solid black line is a linear fit that predicts an uncertainty SE $\sim 0.12$ mm$^{-1}$ with 50 A-lines.](image-url)

![Fig. 10 Goodness-of-fit measures. (a) Adjusted $R^2$ is plotted as a function of parameter estimation method for a single-fibrotic VOI with 240 A-lines. The PL, $\alpha$-T-PL, and IT-PL gave higher adjusted $R^2$ than others. (b) Histogram of RMSE for 111 fibrotic VOIs for $\alpha$-T-PL. More than 90% had good fits with RMSE < 12. (c) Using the same data, over 85% of VOIs have a CV < 0.5.](image-url)
plaques with a diffuse edge (Fig. 12). Typically, this is resolved by experts only after analyzing adjacent frames.

5 Discussion

The characterization of tissue optical properties from 3-D IV-OCT clinical pullbacks will be an important step in reliable tissue classification. Previous methods for estimating optical properties have typically used time-averaged data in a stationary acquisition or single A-lines from a pullback. Since stationary acquisitions are clinically impractical and single A-lines are extremely noisy, we created a 3-D approach whereby groups of A-lines close to each other are analyzed together. Innovations in this report include: use of A-lines from within a 3-D VOI to improve stability of estimates; advanced, robust parameter estimation approaches including goodness-of-fit estimates; and a rigorous methodology for comparing estimation methods applied to clinical pullback data. Results suggest that filtering is desirable, that estimates vary some with the method used, that PL and its variants generally outperformed IL and its variants, and that RMSE is the favored goodness-of-fit measure which can be used effectively to “censor” VOIs with bad fits. As detailed later, we deemed \( \alpha \)-T-PL as best. In general, we can conclude that the PL model, which fits one slope and multiple intercepts to a collection of spatially adjacent A-lines, is appropriate since there should be a single characteristic \( \mu_t \) value and a single slope for locally homogeneous tissue.

Table 2 - Estimates of \( \mu_t \) are consistent with values from two previously reported studies that have estimated optical properties of atherosclerotic plaques using the same imaging system (1310-nm center wavelength and 110-nm wavelength range).

| Tissue type | \( \mu_t \) (estimated) (mm\(^{-1}\)) | \( \mu_t \) (literature) (mm\(^{-1}\)) |
|-------------|----------------------------------------|--------------------------------------|
| Calcified   | 3.84 ± 0.95                            | 2–5                                  |
| Fibrotic    | 2.15 ± 1.08                            | 2–5                                  |
| Lipid       | 9.99 ± 2.37                            | ≥10                                  |

\( \mu_t \) was the best filtering method among those tested. Filtering visually reduced the noise in A-lines. Comparing filters on a single VOI, the uncertainty of \( \mu_t \) was minimized with the LF [Fig. 4(a)]. Also, LF reduced the spread of \( \mu_t \) across many VOIs for a given tissue [Fig. 4(b)], presumably enabling better separation of tissues. We did not observe any consistent bias due to filtering on \( \mu_t \) estimates. It is satisfying that a filter designed for speckle noise gave the best results for parameter estimation because speckle is the dominant noise in OCT images.

Comparing parameter estimation methods via multiple assessments, we determined that PLs and \( \alpha \) trimming were useful and that the best overall method was \( \alpha \)-T-PL. Comparing results on a typical VOI, the uncertainty of \( \mu_t \) was least for \( \alpha \)-T-PL (Fig. 7). Since we are ultimately interested in separating tissue types, reducing the spread of \( \mu_t \) estimates across many VOIs is desirable. \( \alpha \)-T-PL and PL gave a reduced spread of \( \mu_t \) across many VOIs as compared with other methods (Fig. 8, legend). Since results were variable across filters, VOIs, tissue types, and estimation methods, we developed a voting scheme for comparing parameter estimation methods. For each VOI, we picked a winning technique based on two different criteria: (1) the smallest uncertainty SE of \( \mu_t \) estimate, and (2) the smallest RMSE goodness-of-fit for a VOI. We then counted across all VOIs the number of times each technique was a winner and sorted results. Based on criterion (1), we obtained the following ranking of the four best techniques: \( \alpha \)-T-PL > PL > IT-PL > NIL-PL-TM. Based on (2), we obtained the following ranking: IL-PL-TM > \( \alpha \)-T-PL > NIL-PL-TM > \( \alpha \)-T-IL. Since \( \alpha \)-T-PL was in the top two for both criteria, we deemed it best. Although IL-PL-TM had the lowest RMSE, it had a large SE uncertainty [it was not in the top four based on criterion (1)]. It is worth noting that having a smaller SE uncertainty is more significant. This is because sometimes a good numerical fit could be obtained with a high SE. Similarly, \( \alpha \)-T-PL was voted best when we rank-ordered standard deviations across many VOIs of each tissue type. The computational complexity of \( \alpha \)-T-PL can be greatly reduced by saving intermediate calculations.

There have been previous reports of \( \mu_t \) (total attenuation coefficient) and \( \mu_s \) (scattering coefficient) for atherosclerotic tissues in the literature. Our estimates of \( \mu_t \) are consistent with

| Tissue type | TP (literature) | TN (literature) | FP (literature) | FN (literature) | SENSITIVITY (literature) | SPECIFICITY (literature) |
|-------------|----------------|----------------|----------------|----------------|--------------------------|--------------------------|
| (a)         |                |                |                |                |                          |                          |
| Calcium     | 18.4 ± 4.4     | 36.6 ± 5.2     | 4.4 ± 1.7      | 2.8 ± 1.9      | 0.86 ± 0.10              | 0.86 ± 0.05              |
| Lipid       | 17.8 ± 4.3     | 40.4 ± 3.1     | 3 ± 1.6        | 1 ± 0.7        | 0.95 ± 0.04              | 0.93 ± 0.03              |
| Fibrotic    | 19.6 ± 2.3     | 39.2 ± 4.6     | 0.8 ± 0.4      | 2.6 ± 1.7      | 0.89 ± 0.07              | 0.98 ± 0.01              |
| (b)         |                |                |                |                |                          |                          |
| Calcium     | 17.4 ± 5.1     | 32.6 ± 5.3     | 2.8 ± 1.8      | 2.6 ± 0.9      | 0.86 ± 0.05              | 0.92 ± 0.05              |
| Lipid       | 12.8 ± 2.1     | 40.2 ± 2.2     | 2 ± 1          | 0.4 ± 0.5      | 0.97 ± 0.04              | 0.95 ± 0.02              |
| Fibrotic    | 19.8 ± 1.8     | 32.2 ± 1.3     | 1 ± 1          | 2.4 ± 1.8      | 0.89 ± 0.08              | 0.97 ± 0.03              |
Fig. 11 \((\mu_t, \langle I_i \rangle, I_0)\) were used as features in automatic classification of VOIs using an SVM classifier into three plaque types—fibrotic, lipid, and calcium. All three features are plotted in (a) and the two best features are plotted in (b). 311 expert annotated VOIs from 35 IVOCT pullbacks. We used \(\alpha\)-T-PL, LF, and censoring of VOIs with RMSE $> 12$, leaving 277. Feature space indicates a good separation between all three plaque types (calcified, fibrotic, and lipid). The (mean ± std.dev.) of \(\mu_t\) estimates was: calcified \((3.84 ± 0.95 \text{ mm}^{-1})\), fibrotic \((2.15 ± 1.08 \text{ mm}^{-1})\), and lipid \((9.99 ± 2.37 \text{ mm}^{-1})\). Classification results are in Table 3.

Fig. 12 Our robust estimation methods have helped us distinguish between a lipid plaque (a) and a calcified plaque with a diffuse edge (b), both shown by blue arcs. This is often a source of confusion at first glance during manual analysis. When we employed parameter estimation of \(\mu_t\), we could see a significant numerical difference between the two cases (lipid: \(8.62 ± 0.66 \text{ mm}^{-1}\), calcium with diffuse edge: \(2.06 ± 0.23 \text{ mm}^{-1}\)), which we believe would aid in proper classification.
two previously reported studies that have estimated optical properties of clinically obtained atherosclerotic plaques using the same imaging system but different estimation procedures on stationary IVOCT acquisitions\textsuperscript{29,30} (Table 2) \cite{Gargesha et al.: Parameter estimation of atherosclerotic tissue optical properties...} \textsuperscript{32,33} report much lower values of \( \mu _{t} \) for lipid (2.7 \pm 0.8 \text{ mm}^{-1} \) and 3.2 \pm 1.1 \text{ mm}^{-1} \) and much higher values for calcified (11.1 \pm 4.9 \text{ mm}^{-1} \), but these studies used \textit{ex vivo} images, a bench-top OCT scanner, and a different light source, therefore, they are not comparable to our study. Another study at \( \lambda _{0} \) = 1300 nm\textsuperscript{31} reported \( \mu _{t} \) and \( g \) values instead of \( \mu _{t} \) making comparisons difficult.

The robust, 3-D methods proposed here for measuring optical properties of tissue should be applicable to other OCT applications. Specifically, methods should be applicable to volumetric OCT cancer imaging, where optical properties have been used to distinguish cancerous tissues.\textsuperscript{42-44} Because it is desirable to include the quality of assessment with parameter estimates, we investigated goodness-of-fit measures. Adjusted \( R^{2} \) is a good way to compare models of different orders. The PL methods (\( \alpha \)-T-PL, PL, and IT-PL) gave higher adjusted \( R^{2} \) than other methods (Fig. 10), but \( R^{2} \) depends on slope and is inappropriate for assessing the fit in a particular VOI. The CV was considered, but it was determined that the CV simply favored VOIs with more A-lines. We prefer RMSE because it is simple to compute and interpret. A histogram of RMSE across many VOIs [Fig. 10(b)] shows that 90% of VOIs have “good fits” with RMSE \textless 12. Classification results were improved when VOIs with RMSE \textgreater 12 were censored, indicating that the RMSE could be a useful feature for automated processing going forward. For example, one could estimate \( \mu _{t} \) from regions, but additionally use the computed RMSE value as a confidence in the \( \mu _{t} \) estimate and weight the feature accordingly during classification.

The exploratory classification study yielded surprisingly good results based solely on optical property parameters (Table 3, Fig. 11). The choice of classifier and other parameter settings was determined from preliminary optimization experiments in which a small subset of VOIs of all three plaque types was employed. We used SVM, three tissue types, one-against-all training, three features (\( \mu _{t}, I_{1}, I_{2} \), and fivefold cross validation to assess results. Censoring VOI data with poor fits (RMSE \textgreater 12) improved sensitivity and specificity as compared with uncensored data for calcium and lipid VOIs, and only slightly lowered specificity (while keeping the same sensitivity) for fibrotic VOIs [Tables 3(a) versus 3(b)]. It was encouraging that the optical parameter estimates allowed us to distinguish between lipid plaques and calcium plaques with a diffuse edge, often a problem during manual analysis (Fig. 12). In manual analysis, analysts typically analyze adjacent 2-D frames to make a determination using standard definitions provided by Yabushita et al.\textsuperscript{14} It is promising that the computational methods can determine this from optical properties alone.

The aim of our study was to compare advanced parameter estimation methods applicable to clinical 3-D IVOCT pullbacks. This avoids the use of \textit{ex vivo} data with its potential limitations including potential tissue degradation, no mean or pulsating pressure, no cardiac motion, unrealistic temperatures, no blood artifacts, and a straight path pullback rather than actual 3-D coronary geometry. Moreover, in the event of spatially inaccurate, sparse histological sampling, one can make inappropriate “ground truth” determinations using \textit{ex vivo} data. Instead we used as ground truth VOIs identified by well-trained analysts using well-established criteria. Our VOI classification results overestimate that which would be obtained in automatic processing of pullback data. That is, analysts choose homogeneous, easily identified VOIs, giving rise to relatively unambiguous computer classification. In addition, analysts purposely did not choose regions of macrophages and thrombi because we were focusing on optical attenuation estimation rather than other features. Our approach should be quite appropriate for optimizing the 3-D parameter estimation methods in this report.

In summary, we believe that the robust processing methods make it possible to assess tissue optical properties from noisy, IVOCT clinical pullback data. In addition, optical parameters thus obtained will be important image features for an automated analysis of plaques. We believe that the 3-D methods reported here for assessing optical properties will also be applicable in volumetric OCT cancer imaging.

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