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High pressure induced phase transition and superdiffusion in anomalous fluid confined in flexible nanopores

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The behavior of a confined spherical symmetric anomalous fluid under high external pressure was studied with Molecular Dynamics simulations. The fluid is modeled by a core-softened potential with two characteristic length scales, which in bulk reproduces the dynamical, thermodynamical, and structural anomalous behavior observed for water and other anomalous fluids. Our findings show that this system has a superdiffusion regime for sufficient high pressure and low temperature. As well, our results indicate that this superdiffusive regime is strongly related with the fluid structural properties and the superdiffusion to diffusion transition is a first order phase transition. We show how the simulation time and statistics are important to obtain the correct dynamical behavior of the confined fluid. Our results are discussed on the basis of the two length scales. © 2014 AIP Publishing LLC. [http://dx.doi.org/10.1063/1.4897956]

I. INTRODUCTION

The dynamical behavior of fluids at nanoscale has been attracting attention recently. The reason behind this attention is that nanoconfined liquids exhibit hydrodynamic, dynamic, and structural properties different from the mesoscopic confined and bulk systems.1 For instance, the fast flow of the liquids confined in nanostructures cannot be described by the classical hydrodynamic.2–4 This inconsistency between the experiments and the classical theories becomes even more significant in anomalous liquids, such as water,3,4 where the enhanced flow is higher than the enhancement observed in other fluids.2–4 In the particular case of water, this unusual dynamics might lead to important technological applications in desalination.1,3,4

Most of the recent experimental and theoretical studies about confined fluids are related to water. These studies have shown that the confinement produces additional unusual properties such as: the presence of a well defined layered structure,7 crystallization of the contact layers at high temperatures,8–10 the increase of the diffusion coefficient at constant temperature. As well, colloidal systems and globular proteins can also exhibit anomalous properties.34

What are the bulk properties in anomalous fluids that under confinement might lead to the appearance of unusual dynamical effects? Most liquids contract upon cooling. This is not the case of the anomalous liquids. For them the specific volume at ambient pressure starts to increase when cooled below a certain temperature. In addition, while most liquids diffuse faster as pressure and density decreases and contract on cooling, anomalous liquids exhibit a maximum density at constant pressure, and the diffusion coefficient increases under compression.15 The most well known anomalous fluid is water,16–18 but Te,19 Ga, Bi,20 Si,21,22 Ge12Te55,23 liquid metals,24 graphite,26 silica,26–28 silicon,29 BeF2,30 also show the presence of thermodynamic anomalies.18 In addition to water,30,31 silica27–29,32 and silicon33 exhibit a maximum in the diffusion coefficient at constant temperature. As well, colloidal systems and globular proteins can also exhibit anomalous properties.34

The diffusion coefficient, in bulk, is obtained from the scaling factor between the mean square displacement and the exponent of the time, namely, \( \langle r(0)r(t) \rangle \approx t^\alpha \). For the anomalous liquids in the bulk this scale factor follows the Fick diffusion. That means that the mean square displacement is linear with time, \( \alpha = 1 \). As the system becomes confined in addition to the Fickian dynamics two anomalous no-Fickian behaviors are observed. The first, the superdiffusive regime, complies all the \( \alpha > 1 \) cases with a fast dynamics. The limit is an ideal system where the molecules can move with constant velocity and, therefore, ballistic diffusion, \( \alpha = 2 \). The second, the subdiffusive regime, includes dense systems in which the dynamics is slower and the particles move in a chain-like structure and cannot pass each other forming a single-file diffusion with \( \alpha = 0.5 \). The transition between these regimes was observed in fluids confined inside nanotubes, and depends on the radius and length of the nanotube as well as on the time of observation of the movement.11,35 It is not clear, however, how the dynamics is related with the structure.

In this paper we explore the connection between the dynamic and structural anomalous behavior in nanoconfined systems suggesting that the layering structure governs the dynamic transition. We propose that for very high pressures the transition between Fickian to superdiffusive is related with the structural transition between two to three layers.

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The fluid is modeled using a two length scale potential. Coarse graining potentials are a suitable tool to investigate the properties of a general confined anomalous fluids. Recently we have shown that this effective potential is capable to reproduce the enhancement flow and the high diffusion coefficient of nanofluid confined anomalous fluids. For small pressures the structure is related to thermodynamic phase transitions in the wall. The model used in this work exhibits the thermodynamic, dynamic, and structural anomalous behavior in bulk and in confinement systems. The paper is organized as follows: in Sec. II we introduce the model and describe the methods and simulation details; the results are given in Sec. III; and in Sec. IV we present our conclusions.

II. THE MODEL AND THE SIMULATION DETAILS

A. The model

The anomalous fluid was modeled as spherical core-softened particles with mass \( m \) and effective diameter \( \sigma \). The interaction is obtained by the potential

\[
\frac{U(r_{ij})}{\varepsilon} = 4 \left[ \left( \frac{\sigma}{r_{ij}} \right)^{12} - \left( \frac{\sigma}{r_{ij}} \right)^{6} \right] + u_0 \exp \left[ -\frac{1}{\sigma^2} \left( \frac{r_{ij} - r_0}{\sigma} \right)^2 \right],
\]

where \( r_{ij} = |\vec{r}_i - \vec{r}_j| \) is the distance between the two fluid particles \( i \) and \( j \). This equation has two terms: the first one is the standard 12-6 Lennard-Jones (LJ) potential and the second one is a gaussian centered at \( r_0 \), with depth \( u_0 \) and width \( c_0 \). Recent studies suggest that simple Gaussian fluids are able to reproduce the thermodynamic anomalies observed in water. Using the parameters \( u_0 = 5.0, c = 1.0, \) and \( r_0/\sigma = 0.7 \) this equation represents a two length scale potential, with one scale at \( r_c \approx 2\sigma \), where the force has a local minimum, and the other scale at \( r_c \approx 2\sigma \), where the fraction of imaginary modes has a local minimum. The potential is shown in Fig. 1(a). Our core-softened model, introduced to study bulk systems, does not have any directionality and therefore it is not water. However, despite the mathematical simplicity, it does exhibit the density, the diffusion, and the response functions anomalies observed in water, as well as confined water properties.

These suggest that some of the anomalous properties that are attributed to the directionality of water can be found in spherical symmetry systems.

It was already shown that the confined fluid properties are strongly affected by the nanopore mobility. Since we want to fix the pressure at high values, we explore behavior of this anomalous fluid confined in a non-rigid nanopore. The nanopore was modeled as two parallel flat plates. The simulation box is a parallelepiped with dimensions \( L_x \times L_y \times L_z \). The model for the fluid-wall system is illustrated in Fig. 1(b). Two walls, \( A \) in the top and \( B \) in the bottom, are placed in the limits of the \( z \)-direction of the simulation box. The sizes \( L_x \) and \( L_y \) are fixed in all simulations, and defined as \( L_x = L_y = L = 40\sigma \). This value for \( L \) was chosen to ensure that will be enough area in the plates to all particles used in our simulations be disposed. The values of \( L_z \) depend on the applied pressure \( p_z \) in the \( z \)-direction. The system was modeled in the NAP-T ensemble using the Lushkovich and van Smol method of fluctuating confining walls to fix \( p_z \).

The walls are flat and purely repulsive, and the interaction between a fluid particle and these walls is represented by the Weeks-Chandler-Anderson (WCA) potential

\[
U^{WCA}(z_{ij}) = \begin{cases} 
U_{LJ}(z_{ij}) - U_{LJ}(z_c), & z_{ij} \leq r_c, \\
0, & z_{ij} > r_c.
\end{cases}
\]

Here, \( U_{LJ} \) is the standard 12-6 LJ potential, included in the first term of Eq. (1), and \( r_c = 2/\sigma \) is the usual cutoff for the WCA potential. Also, the term \( z_{ij} \) measures the distance.
between the wall at \( j \) position and the \( z \)-coordinate of the fluid particle \( i \).

### B. The simulation details

The physical quantities are computed in the standard LJ units,\(^{45} \)

\[
r^* \equiv \frac{r}{\sigma}, \quad \rho^* \equiv \rho \sigma^3, \quad \text{and} \quad t^* \equiv t \left( \frac{\epsilon}{m \sigma^2} \right)^{1/2}, \quad (3)
\]

for distance, density of particles, and time, respectively, and

\[
p^* \equiv \rho \sigma^3 \quad \text{and} \quad T^* \equiv \frac{k_B T}{\epsilon} \quad (4)
\]

for the pressure and temperature, respectively. Since all physical quantities are defined in reduced LJ units in this paper, the \( * \) is omitted, in order to simplify the discussion.

The simulations were performed at constant number of particles, constant \( N = L_x \times L_y \), constant perpendicular pressure and constant temperature (\( N \) constant ensemble). The perpendicular pressure was fixed using the Lupkowski and van Smol method.\(^{52} \) In this technique, the nanopores walls had translational freedom in the \( z \)-direction, acting like a piston in the fluid, and a constant force controls the pressure applied in the confined direction. This translational freedom induces vibrational effects in the nanopore. However, the wall moves as one particle of area \( L_z^2 \) in the \( xy \) plane and thickness \( \sigma_w \) in the \( z \) direction. Then this vibrational effects are distinct from the case of atomistic detailed walls, where all particles vibrate. This scenario is similar to some recent experiments on water confined inside nanopores at externally applied high pressures\(^{54,55} \) and includes the nanopore flexibility. It has been shown that the anomalous fluid behavior inside rigid nanopores is different from flexible nanopores,\(^{36,37} \) and in this paper we address the second case.

Considering the nanopore flexible walls, the resulting force in a fluid particle is then

\[
\vec{F}_R = -\nabla U + \vec{F}_{i A} + \vec{F}_{i B}, \quad (5)
\]

where \( \vec{F}_{i A/B} \) indicates the interaction between the particle \( i \) and the wall \( A/B \). Since the walls are non-rigid and time-dependent, we have to solve the equations of motion for \( A \) and \( B \),

\[
m_w \ddot{\vec{r}}_{A/B} = p_z S_w \vec{a}_{A/B} - \sum_{i=1}^{N} \vec{F}_{i A/B}(\vec{r}_{i A/B}), \quad (6)
\]

where \( m_w \) is the piston mass, \( p_z \) is the applied pressure in the system, \( S_w \) is the wall area, and \( \vec{a}_{A/B} \) is an unitary vector in positive \( z \)-direction, while \( \vec{a}_{B} \) is a negative unitary vector. Both pistons \((A\text{ and }B)\) have mass \( m_w = m \), width \( \sigma \), and area equal to \( S_w = L_z^2 \).

The system temperature was fixed using the Nose-Hoover heat-bath with a coupling parameter \( Q = 2 \) and was varied from small temperatures, \( T = 0.01 \) to higher temperatures \( T = 0.4 \). Standard periodic boundary conditions were applied in the \( x \) and \( y \) directions. The equations of motion for the fluid particles and the walls were integrated using the velocity Verlet algorithm, with a time step \( \delta t = 0.001 \).

Five independent runs were performed to evaluate the properties of the confined fluid. The initial system was generated placing the fluid particles randomly in the space between the walls. The initial displacement for the simulations was \( L_z = 15 \). We performed \( 5 \times 10^5 \) steps to equilibrate the system. This equilibration time was taken in order to ensure that the walls reached the equilibrium position for the fixed values of \( p_z \). These steps are then followed by \( 1 \times 10^5 \) steps for the results production stage. The large production time is necessary to observe the correct dynamical behavior of the confined fluid.

The fluid-fluid interaction, Eq. (1), has a cutoff radius \( r_{\text{cutoff}} = 3.5 \). The number of particles was fixed in \( N = 1000 \), and four values of pressure were simulated: \( p_z = 7.0, 8.0, 9.0, \) and \( 10.0 \). Due to the excluded volume originated by the nanopore-fluid interaction, the distance \( L_z \) between the walls needs to be corrected to an effective distance,\(^{56,57} \) that can be approximated \( L_{\text{eff}} \approx L_z - 1 \). The effective distance, due the nanopore flexibility, will oscillate around an average value \( L_{\text{eff}} \) and the average density will be \( \rho = N/(L_{\text{eff}} L_z^2) \). Also, it is important to reinforce that, since \( N \) is fixed for all simulations, the distinct values for density are obtained by the variation in pressure and temperature, and consequently variation in plates separation, \( L_z \).

To study the fluid dynamical properties we analyse the relation between the mean square displacement with time, as follows:

\[
\langle (\vec{r}_i(t) - \vec{r}_i(t_0))^2 \rangle = \Delta \langle (\vec{r}_i(t))^2 \rangle = 4 D t^\alpha, \quad (7)
\]

where \( \vec{r}_i(t_0) = (x(t_0), y(t_0), z(t_0))^1/2 \) and \( \vec{r}_i(t) = (x(t)^2 + y(t)^2 + z(t)^2)^1/2 \) denote the parallel coordinate of the confined anomalous fluid particle at a time \( t_0 \) and at a later time \( t \), respectively. We should address that the mean square displacement was calculated considering all the particles in the system. Nanoconfined fluids assume a layered structure. Despite this, the evaluation of \( 4 D t^\alpha \) for each layer can lead to a spurious statistics for the result, since the number of particles in each layer is small and the particles can move from one layer to another, leading to a poor time average in Eq. (7). Depending on the scaling law between \( \Delta \langle r_i(t)^2 \rangle \) and \( t \) in the limit \( t \rightarrow \infty \), different diffusion mechanisms can be identified: \( \alpha < 1.0 \) refers to a subdiffusive regime, with \( \alpha = 0.5 \) identifying a single file regime,\(^{11} \) \( \alpha = 1.0 \) stands for a Fickian diffusion whereas \( \alpha > 1.0 \) defines the superdiffusive regime, and \( \alpha = 2.0 \) refers to a ballistic diffusion.\(^{12,35} \)

In order to define the fluid characteristics at different distances from the nanopore walls, the structure of the fluid layers was analyzed using the radial distribution function \( g(r_i) \), defined as\(^{56,57} \)

\[
g(r_i) = \frac{1}{\rho^3 V} \sum_{i \neq j} \delta(r - |r_i - r_j|) \left( \theta(|z_i - z_j|) - \theta(|z_i - z_j| - \delta z) \right). \quad (8)
\]

where the Heaviside function \( \theta(x) \) restricts the sum of particle pair in a slab of thickness \( \delta z = 1.0 \) close to the wall or \( \delta z = 1.0 \) away from the walls.

In all simulations the mean variation in the system size induced by the wall fluctuations is smaller than 2%. Data
nanopores. The number of layers depends on the different nanopores geometry and size. Since the number of particles in our system is fixed, the density change observed in Figure 2 implies change in the distance between the two plates and consequently in the number of layers.

For $p_z = 7.0$, the fluid has three layers for all the temperatures studied as shown in Fig. 3(b).

The transition from low to high density as the temperature is increased at constant pressure is quite counterintuitive. Usually the increase of density is associated with decrease of entropy. Here, however, it is the contrary. This anomalous behavior follows from the same mechanism of the increase of density at constant pressure, the bulk density anomaly.

At low temperatures, particles in the same layer minimize the energy, Eq. (1), by being at a distance $r_z \approx 1.2$, the first length in the potential, as shown in Fig. 4. When the pressure is high and the temperature is sufficient high, the central layer melts and the distance between the planes is smaller than any of the two length scales.

At these low temperatures both the contact planes are quite structured, as shown in Fig. 4(a) for the temperatures $T = 0.01$, 0.04, 0.075, and 0.2, where the fluid is structured in 3 or 2 layers. The central plane is solid-like, as illustrated in Fig. 4(b) for $T = 0.045$, where we compare the central and contact layer structure. These structures, similarly to the low temperature liquid water, have low density but high order and, consequently, low entropy. As the temperature is increased, the central layer melts. The two contact layers approach, being at the first length scale, with a distance $r_z \approx 1.2$ from each other, as shown in Fig. 3(a). Inside each, the layer particles are at $r_z \approx 2$ distant from each other. As the temperature is increased, the order inside each layer decreases, as shown in Fig. 4(a), and the entropy increases. Therefore, the denser system is more entropic, similarly to what happens with anomalous fluids at the region of the density anomaly.
What is the relation between this layer transition and the mobility of the nanoconfined particles? The layers structure can provide both a restriction or an enhancement of the mobility of the particles.\textsuperscript{37, 42, 44} In order to illustrate this point we study the parallel mean square displacement (MSD) as a function of time for different temperatures and pressures. Fig. 5(a) shows the MSD versus time for $p_z = 10.0$ and $T = 0.01, 0.045, 0.05, 0.2$. In order to understand the behavior of the mobility in the framework of Eq. (7), the exponent $\alpha$ is computed in all the studied cases. A Fickian diffusion was observed for $p_z = 8.0, 9.0, \text{and } 10.0$ for temperatures above the three-to-two layers transition. This behavior was obtained after long time simulation. For shorter simulation times the system exhibits an apparent subdiffusive regime, where $\alpha < 1.0$. This behavior was also obtained for water confined in nanotubes.\textsuperscript{35} For our model, as $t \to \infty$ (see Fig. 5(a)) the Fickian diffusion is recovered. As example, we show in the purple curve of Fig. 5(a) the behavior for $T = 0.05$ and $p_z = 10.0$.

For lower temperatures, below the three-to-two layer transition, however, the systems for $p_z = 8.0, 9.0$ and $10.0$ exhibit a superdiffusive behavior with $\alpha > 1$.

Fig. 5(b) shows the behavior of $\alpha$ versus temperature, illustrating that the transition temperature from non-Fickian to Fickian regime coincides with the transition from three-to-two layers and with the increase of density shown on Fig. 2.

The transition between layers followed by change in the exponent $\alpha$ was also observed in atomistic models for water.\textsuperscript{11, 35} In these cases, it is not clear if the anomalous diffusion is in equilibrium or if it is an artifact of the short simulation times. In our case, the coarse grained potential provides us with an easy way to perform long simulations and we can ensure that the system is equilibrated.

IV. CONCLUSION

We have studied the behavior of an anomalous fluid confined inside a flexible nanopore at high external pressure. Our results show a structural phase transition in the $\rho \times T$ phase diagram for isobaric curves with $p_z \geq 8.0$. This phase transition corresponds to a three-to-two layers transition, and it is associated to a transition between a superdiffusive regime and a Fickian diffusion. These results indicate that anomalous fluids can exhibit a superdiffusion regime at small temperature and high pressures associated with the same mechanism that at the bulk generate the density anomaly.
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