Blast-wave model description of the HBT radii measured in $pp$ collisions at the LHC energies

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Blast-wave model is applied to describe the Hanbury-Brown–Twiss (HBT) radii of pionic systems produced in $pp$ collisions at the LHC energies.

PACS numbers: 25.75.Gz, 25.75.Ld

Dedicated to Professor Jan Pluta on the occasion of his 70th birthday

1. Introduction

At very high energies, such as those presently available at the LHC, the final state hadron multiplicities in $pp$ collisions become large and hydrodynamic description of hadron production in these processes may become possible in the similar way as in peripheral heavy-ion collisions [1, 2, 3]. Following this expectation, in this conference proceedings I use the hydro-inspired, blast-wave model to analyse the ALICE data on pion correlation functions [4]. This work highlights some of the recent results obtained together with A. Bialas and K. Zalewski [5, 6, 7].

2. Blast-wave model

I use the most common version of the blast-wave model [8, 9, 10, 11]. At freeze-out, pions are created at a fixed proper time $\tau = \tau_f = \sqrt{t^2 - z^2}$. Then, the single-particle source function becomes

$$w(k, x) = k_0 \cosh \eta e^{-U \cosh \eta + V \cos \phi} f(r),$$

where $k_0 = (m^2 + k_{\perp}^2)^{1/2}$ is the pion energy (with $m$ and $k_{\perp}$ being the pion mass and transverse momentum, respectively), while $\eta, \phi$ and $r$ are

* Presented at the XI Workshop on Particle Correlations and Femtoscopy, November 3-7, 2015, Warsaw, Poland
Table 1. Model parameters determined for different multiplicity classes (the highest multiplicity class has been omitted).

| mult. class | 1–11 | 12–16 | 17–22 | 23–28 | 29–34 | 35–41 | 42–51 |
|-------------|------|------|------|------|------|------|------|
| $\langle N_c \rangle$ | 6.3  | 13.9 | 19.3 | 25.2 | 31.2 | 37.6 | 45.6 |
| $R$ [fm]     | 1.15 | 1.52 | 1.77 | 1.97 | 2.14 | 2.32 | 2.49 |
| $\tau_f$ [fm] | 1.90 | 2.18 | 2.37 | 2.50 | 2.63 | 2.74 | 2.80 |
| $\chi^2$     | 0.96 | 1.90 | 2.89 | 4.06 | 5.88 | 5.45 | 11.63 |
| $\chi^2_{\text{tot}}$ | 18.77 | 11.08 | 6.34 | 4.86 | 6.65 | 5.79 | 11.72 |

the space-time rapidity, azimuthal angle and transverse distance from the symmetry axis. I also use the notation $U = \beta k_0 \cosh \theta$ and $V = \beta k_\perp \sinh \theta$, with $T = 1/\beta$ being the freeze-out temperature. The function $\theta$ describes the Hubble-like transverse flow $\sinh \theta = \omega r$, with $\omega$ being a parameter [12].

The function $f(r)$ defines the transverse profile/density of the source. It turns out that the model can describe the HBT radii measured by the ALICE collaboration if the function $f(r)$ is taken in the form

$$f(r) \sim e^{-(r-R)^2/\delta^2}$$

(2)
corresponding to a "shell" of the width $\sqrt{2}\delta$ and the radius $R$ [6]. Thus, the model contains altogether five free parameters: $T$, $\omega$, $\tau_f$, $R$ and $\delta$, which may depend on the multiplicity of the event. The freeze-out temperature is set equal to $T = 100$ MeV and the width of the shell is taken as $\delta = 0.75$ fm. The measured average transverse momentum, taken from CMS [13], fixes (for each multiplicity bin) the relation between $\omega R$ and the ratio $R/\delta$. In this way, one is left with the two free parameters: $R$ and $\tau_f$, which are fitted with the $\chi^2$ method. The model parameters and $\chi^2$ values determined for various multiplicity classes are shown in Table 1. The number of degrees of freedom is 13, $\chi^2$ excludes the first bin in $k_\perp$, while $\chi^2_{\text{tot}}$ includes all the bins.

3. Correlation functions

The Bose-Einstein correlation function of two identical particles is defined as the ratio of the two-particle distribution and the product of the one-particle distributions [14]. In our model it is given by the formula [5, 6]

$$C(p_1,p_2) = 1 + \frac{\tilde{w}(P_1;Q)\tilde{w}(P_2;-Q)}{w(p_1)w(p_2)} = 1 + \frac{|\tilde{w}(P_1;Q)|^2}{w(p_1)w(p_2)}.$$  

(3)

1 All irrelevant constants are cancelled in the definition [1]
Here one uses the definition

\[ \tilde{w}(P_{12}; Q) = \int dx \: e^{iQx} w(P_{12}; x), \quad w(p) = \int dx \: w(p; x), \]

where \( P_{12} = (p_1 + p_2)/2 \) and \( Q = (p_1 - p_2) \). For boost-invariant and cylindrically symmetric systems, the average three-momentum of a pair may be set along the \( x \) axis (the “out” direction). The remaining two orthogonal directions are denoted as the “long” and “side” directions. The HBT radii are the logarithmic derivatives of the correlation functions calculated along these three directions for \( Q \to 0 \) [14].

An example of our results, obtained for the multiplicity class 23–28 for the “side” and “out” directions, is shown in Table 2. The agreement between the model results and the data is very good. Interestingly, one can reproduce the values of the radius \( R_{\text{out}} \) that becomes smaller than \( R_{\text{side}} \) for large values of \( P_\perp \). This behaviour reminds the HBT puzzle discussed in the context of heavy-ion collisions [15, 16]. One can check that in our case, the crucial ingredient of the model, responsible for the correct description of the ratio \( R_{\text{out}}/R_{\text{out}} \), is the “shell” structure described by the density profile (2). This finding is similar to the observation made in [17] where the data [18] has been analysed.

### 4. Closing remarks

In this conference contribution I have given further evidence that pions produced in high-energy \( pp \) collisions originate from a thermally equilibrated, expanding source.

Let me note that various attempts to interpret hadron production within thermal and statistical models have been the subject of a very successful
collaboration between Krakow theoretical and Warsaw experimental groups, which was initiated by Professor Jan Pluta at the beginning of 2000s. Our intense scientific contacts led to the construction of the Therminator code [19] and to many papers discussing various aspects of femtoscopy [20], including the HBT puzzle [15]. During the WPCF 2015 Workshop we have celebrated Jan’s 70th birthday. I hope Jan will remain in good shape, very active, and full of inspiring ideas for our community in the following years.

Acknowledgments: This work has been supported in part by Polish National Science Center Grant No. DEC-2012/06/A/ST2/00390.

REFERENCES

[1] L. Ferroni and F. Becattini, Eur. Phys. J. C 71, 1824 (2011).
[2] P. Bozek, W. Broniowski and G. Torrieri, Phys. Rev. Lett. 111, 172303 (2013).
[3] P. Ghosh, S. Muhuri, J. K. Nayak and R. Varma, J. Phys. G 41, 035106 (2014).
[4] K. Aamodt et al. [ALICE Collaboration], Phys. Rev. D 84, 112004 (2011).
[5] A. Bialas, W. Florkowski and K. Zalewski, Acta Phys. Pol. B 45, 1883 (2014).
[6] A. Bialas, W. Florkowski and K. Zalewski, J. Phys. G 42, 045001 (2015).
[7] A. Bialas, W. Florkowski and K. Zalewski, Phys. Lett. B 748, 9 (2015).
[8] P. J. Siemens and J. O. Rasmussen, Phys. Rev. Lett. 42, 880 (1979).
[9] E. Schnedermann, J. Sollfrank and U. W. Heinz, Phys. Rev. C 48, 2462 (1993).
[10] W. Florkowski and W. Broniowski, Acta Phys. Polon. B 35, 2895 (2004).
[11] F. Retiere and M. A. Lisa, Phys. Rev. C 70, 044907 (2004).
[12] M. Chojnacki, W. Florkowski and T. Csorgo, Phys. Rev. C 71, 044902 (2005).
[13] CMS Collaboration, S. Chatrchyan et al. Eur. Phys. J. C 72, 2164 (2012).
[14] M. A. Lisa, S. Pratt, R. Soltz and U. Wiedemann, Ann. Rev. Nucl. Part. Sci. 55, 357 (2005).
[15] W. Broniowski, M. Chojnacki, W. Florkowski and A. Kisiel, Phys. Rev. Lett. 101, 022301 (2008).
[16] S. Pratt, Phys. Rev. Lett. 102, 232301 (2009).
[17] T. Csorgo, Heavy Ion Phys. 15 (2002) 1; Acta Phys. Pol. B37 483 (2006).
[18] NA22 Coll., N. M. Agababyan et al., Phys. Lett. B422 (1998) 359. See also W. Kittel and E. A. De Wolf "Soft multihadron interactions", (World Scientific, 2005), p. 572.
[19] A. Kisiel, T. Taluc, W. Broniowski and W. Florkowski, Comput. Phys. Commun. 174, 669 (2006); M. Chojnacki, A. Kisiel, W. Florkowski and W. Broniowski, Comput. Phys. Commun. 183, 746 (2012).
[20] A. Kisiel, W. Florkowski, W. Broniowski, and J. Pluta, Phys. Rev. C 73, 064902 (2006).