Optimal Method for Detecting Collusive Saboteur Smart Meters in Smart Grid

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Abstract

Smart grid is a system in which it is possible to use voting-based techniques to resist sabotage of several cyber-attacks. The adaptation of these techniques can be difficult and useless in the case when the malicious resources (i.e., smart meters) of this system can return wrong data in same time; however, the collusion problem is triggered. To detect and resolve the collusive issue, spot-checking technique has been proposed by sending randomly certain number of spotter queries to chosen resources with known correct data in order to estimate resource credibility based on the returned data. This work proposes an original method that resist against collusion attacks by using probability to solving a new spot-checking optimization problem for smart grid systems, with the objective to minimize probability of accepting wrong data (PAWD) while respecting an expected overhead constraint. The proposed solution contains an optimal combination of several parameters, the number of spotter queries sent, the number of resources tested by each spotter query, and the number of resources assigned to run the genuine query. The
optimization procedure includes a new method for evaluating performance metrics of PAWD and expected overhead in terms of the total number of query assignments. To demonstrate the proposed optimization problem and solution procedure, we have provided several illustrative examples.

**Keywords:** Smart grid, smart meters, cyber-security, vulnerability, data-integrity, probability, optimization.

**Abbreviations**

- SGN: smart grid
- MSM: malicious smart meters
- PAWD: probability of accepting wrong data

**Nominations**

- $S_i$: number of smart meters remained in the SGN list after running $i$ spotter queries
- $M_i$: number of smart meters remained in the MSM list after running $i$ spotter queries
- $Q$: number of spotter queries
- $T$: number of smart meters tested in each spotter query
- $G$: number of smart meters assigned to run genuine query
- $E_{Sp}$: expected number of spotter query assignments during the sending of spot-queries
- $E_{Gu}$: expected number of genuine query assignments
- $E$: total expected number of query assignments ($E = E_{Sp} + E_{Gu}$)
- $E_m$: maximum expected number of query assignments
- $SQ_n$: probability that exactly $n$ MSMs are detected during the spot-query-sending process
- $C(G,m)$: conditional PAWD given that $m$ MSMs are chosen for the genuine query
- $P_i(n)$: probability that exactly $n$ MSMs are detected after completion of $i$ spotter queries
- $D_e$: detection error, probability that the smart meters will be not detected after spotter queries.
- $W$: PAWD
1 Introduction

Smart grid (Figure 1) offers a platform to execute intensive tasks by different shared resources, such as smart meters, in a distributed and parallel manner that makes it vulnerable to sabotage attacks. However, these sabotage attacks can be performed by data modification, data destruction and false data injection [1, 2]. The smart grid resources manipulation might be sabotaged by injecting false data and by attempting to get favourable results by accessing smart meters’ applications and by modifying the generated data. This may have various effects such as changing the price of electricity consumed, decreasing the amount of electricity consumed or even causing a blackout. Thus, smart grid security requirements are really very high in spite of several existing of security mechanisms to provide confidentiality, to secure communication between all smart grid resources, and to provide the integrity of the data generated by smart meters.

Nowadays, several sabotage-tolerance techniques have been applied in many grid platforms such as volunteer computing systems [3, 4], desktop grids [5–7], and peer-to-peer grids [8–10], to deal with the verification of the reliability of job results in various grid systems. Voting-based techniques using spot-checking are the most applied ones to resist sabotage, assuring or at least improving reliability of computations and returned data [3], such
as majority voting, m-first voting [11] and credibility-based voting [3] with reputation system [12]. However, these techniques rely on the assumption that the grid resources behave independently which is not valid where a number of collusive resources (smart meters in our work) collectively return the same wrong result (data in our work). Furthermore, sometimes the decision of voting-based techniques may not be exact as cited in [13–16]. Therefore, one group of smart meters in a smart grid might develop some form of collective misbehaviour to sabotage the circulated data by returning a wrong data that is considered the same wrong results in our work, failing the voting mechanism [17–20]. In fact, in order to deal with this threat it is necessary to explore the sabotage-tolerant techniques against collusive smart meters in a smart grid.

To deal with collusion attacks, various approaches have been proposed, for example, there are approaches based on credibility [3, 9, 21], scheduling and certification [14, 22], reputation systems [12, 13, 16], and graph clustering [23]. To the best of our knowledge, no work has been realized by using probability to optimize the spot-checking policy to test the integrity of the data sent by smart meters, taking into account expected overhead for smart grid systems under the collusion attacks.

This work precedes other work, an overview of smart grid cyber-security [24]. Then it gives a new method by formulating and solving a new spot-checking optimization problem in smart grid, which finds an optimal combination of query distribution parameters including the number of deployed spotter queries, the number of smart meters tested by each spotter query, and the number of smart meters assigned to perform the genuine query. The objective of this optimization problem is to minimize probability of accepting wrong data (PAWD) taking into account on expected overhead.

The rest of the paper is organized as follows. Section 2 presents the system model and the problem to be addressed in this work. Section 3 describes the algorithm proposed for evaluating system performance metrics of PAWD and expected overhead. Section 4 presents the formulation of the considered optimization problems. Section 5 gives illustrative examples to demonstrate the proposed optimization problems. Finally, section 6 presents the conclusion of the work.

2 System Model and Problem Statement

In this section, we define our proposed system model, in which we describe all their components. In other hand, we describe in details the statement problem that to be dealt in this paper.
2.1 System Model

The smart grid (Figure 1) is an emerging technology that is revolutionizing the conventional electric grid by providing new services based mainly on Information and Communication Technologies (ICT) [14]. This is a very complex network for energy generation, transmission, distribution and consumption.

In Figure 2, we show the basic components of a smart grid system, which consists of N Smart meters. Each Smart meter is connected to a several local devices or appliances, which are able to communicate with other smart meters via a home area network (HAN). These smart meters analyze and measure data about energy usage, number of appliances, energy pricing, etc. and stores all these data periodically. In addition, these stored data must be returned to a Supervisory Control and Data Acquisition (SCADA) Center in order to monitor and control these collected data in real-time, and provide high security information communication between users and utilities.

The quantity of the energy consumed in a location is calculated by the smart meter linked to this location, taking into account the price of the energy on the market during the specific time of this consumption. In addition, the HAN can supply and sell extra energy to the power grid in order to benefit from high-energy prices in electricity markets that encourage competition among power suppliers [24].

Figure 2 Basic components of a smart grid.
2.2 Problem Statement

In smart grid, malicious attackers or users who can trigger security attacks to its infrastructure, knowing that the attacker tries to corrupt as many smart meters as possible, but its capability is limited. The new approach we propose, has the objective to minimize probability of accepting wrong data (PAWD), and is based on a spot-checking technique.

In our grid, we focus on smart meters attacks that compromise the provided resources and services by exploiting some of their vulnerabilities. In this attack model, we have an adversary, which can compromise the smart meters, and instruct them to behave maliciously to tamper their data and to return wrong data to the SACDA control center. We assume that all malicious smart meters always collude with one another to return incorrect data, the “honest” smart meters always produce the same correct data for the same query at the same time t, and the SCADA control center sends randomly queries to smart meters to return their data at a time t. The smart meter memory stores both their data at random instances, and all data sent to the SCADA control center.

At first, SCADA control center sends the query 0 to all smart meters of SGN and stores the received data in order to initialize the data to be tested in the next query. Then, when a smart meter receives one of these queries, it executes respectively the following tasks:

- Step 1. It captures existing data at the same time t;
- Step 2. It returns this data captured at this time t and those stored at the time $t - 1$ (stored in the memory of the smart meter);
- Step 3. It stores the data captured at this time t in its memory.

Then, the SCADA control center receives the data sent by the smart meters, stores the data captured at time t, and checks whether the data captured at instant $t - 1$ is identical to the data already stored. If the data sent at time t and those sent at time $t - 1$ by the same SM and for the same request are the same, SCADA considers them as correct data and it stores them, otherwise, it considers them as wrong data and it refuses them. The new method we propose, has the objective to minimize probability of accepting wrong data (PAWD).

The smart grid consists of a static set of S0 smart meters, M0 of which are malicious. The malicious smart meters collude in producing wrong data to reduce the efficiency of the voting-based technique against sabotage. To detect the colluding malicious smart meters (MSM), the SGN sends Q spot-checking (spotter) queries with known output data to randomly chosen
smart meters. In addition, the SGN cannot distinguish genuine and spotter queries and, therefore, generate to any query identical wrong outputs data.

In our grid, each spotter query \( i \) is sent to \( T \) smart meters, where \( T \) is a predetermined parameter. The smart meters for each spotter queries are chosen independently. If several smart meters produce identical wrong output data for the \( i \)-th spotter query, they are detected as MSMs and removed from the list of smart meters. Thus, after the \( i \)-th spotter query the list contains \( S_i \leq S_0 \) smart meters, \( M_i \leq M_0 \) of which are MSMs. Then a new \( i + 1 \)-th spotter query is sent to \( T \) smart meters. Let \( G \) represent the number of smart meters assigned to perform the genuine query. After completing \( Q \) spotter queries, the genuine query is sent to \( G \) smart meters randomly chosen from the list of \( S_Q \) remaining smart meters. The data that gets the majority of votes is accepted. If the wrong output data of the genuine query is accepted, the genuine query fails.

The problem addressed in this work is to find the combination of queries distribution policy parameters \( T, G \) and \( Q \) that minimizes the PAWD subject to constrained expected overhead. The overhead is proportional to the total number of queries assignments including the spotter query and the genuine query assignments.

### 3 Algorithm for PAWD Evaluation

Before the assignment of the \( i \)-th spotter query, the list contains \( S_{i-1} \) smart meters, \( M_{i-1} \) of which are MSMs. The probability that \( m \) MSMs are among \( M_{i-1} \) smart meters randomly chosen for the \( i \)-th spotter query is:

\[
SQ(S_{i-1}, M_{i-1}, T, m),
\]

where

\[
SQ(a, b, c, d) = \frac{C_d^{c-d}C_{a-b}^c}{C_a^c}, \quad \text{if } c \geq d
\]

\[
SQ(a, b, c, d) = 0, \quad \text{if } c < d
\]

and \( m \) can vary from 0 to \( T \).

Let \( P_i(m) \) represent the probability that exactly \( m \) MSMs are detected after completion of \( i \) spotter queries. Initially there are \( S_0 \) smart meters in the list with \( M_0 \) of them being MSMs.

Thus,

\[
P_i(m) = SQ(S_0, M_0, T, m)
\]
Therefore, for $1 < i \leq Q$:

$$P_i(m) = \sum_{v=0}^{m} P_{i-1}(v) \cdot SQ(S_0 - v, M_0 - v, T, m - v) \quad (4)$$

Finally, $P_Q(m)$ for $m = 0, \ldots, M_0$ gives the probability that $m$ MSMs are detected after the spot-checking procedure after $Q$ queries.

On the other hand, the probability that the smart meters will not be detected is defined as follow:

$$D_e = 1 - P_Q(m) \quad (5)$$

In addition, the expected number of assignments during the $Q$ spotter queries executions is:

$$E_{Sp}(T, Q) = T + \sum_{i=2}^{Q} \left( \sum_{m=0}^{M} P_{i-1}(m) \cdot T \right) \quad (6)$$

And, the expected number of assignments during the $Q$ spotter query executions is:

$$E_{Gu}(G, T, Q) = \sum_{m=0}^{M} P_Q(m) \cdot G \quad (7)$$

According to the expressions above, the distribution of the number of detected MSMs after the execution of $Q$ spotter queries and the expected number of assignments during the spot-checking can be obtained using the following procedure (Algorithm 1).

If after the spot-checking procedure $m$ MSMs are detected, the SGN sends the genuine query to $G$ out of $S_0 - m$ remaining smart meters with $M_0 - m$ of them being MSMs. The probability that $w$ out of $G$ chosen smart meters are MSMs is:

$$SQ(S_0 - m, M_0 - m, G, w), \quad (8)$$

If $w$ MSMs and $G - w$ honest smart meters are chosen, the wrong output data can be accepted if $w > G - w$. Thus, the conditional probability of accepting wrong data (PAWD) given that $w$ MSMs are chosen for the genuine query is:

$$C(G, w) = \begin{cases} 0, & \text{if } w > G/2 \\ 1, & \text{if } w \leq G/2 \end{cases} \quad (9)$$
Algorithm 1: For detecting MSMs and the expected number of assignments

1. Begin
2. For m = 0 to M do
3. \[ \text{set } P_1(m) = SQ(S_0, M_0, T, m); \]
4. End For
5. **E**_{Sp} = T;
6. For j = 2 to Q do
7. \[ \text{For } l = 0 \text{ to } M_0 \text{ do} \]
8. \[ \text{set } P_j(l) = 0; \]
9. End For
10. **E**_{Sp} = 0;
11. For i = 0 to M_0 do
12. \[ \text{For } k = 0 \text{ to } i \text{ do} \]
13. \[ \text{set } P_j(i) = P_j(i) + P_{j-1}(k) \cdot SQ(S_0 - k, M_0 - k, T, i - k); \]
14. End For
15. End For
16. End For
17. End

The conditional PAWD given that m MSMs are detected is:

\[ \sum_{w=0}^{G} SQ(S_0 - m, M_0 - m, G, w) \cdot C(G, w) \quad (10) \]

Thus, the overall PAWD is:

\[ W(T, G, Q) = \sum_{m=0}^{M_0} \left( P_Q(m) \cdot \sum_{w=0}^{G} SQ(S_0 - m, M_0 - m, G, w) \cdot C(G, w) \right) \quad (11) \]

Notice that the algorithm above can be used to model a situation where the MSMs cannot distinguish spotter and genuine queries.

4 Optimization Problem Formulation

Based on estimation of attack parameter M_0, the SGN can solve the following optimization problem: find T, G and Q that minimize W(G,T,K) s.t. overhead constraint:

\[ E(G, T, Q) = E_{Sp}(T, K) + E_{Gu}(G, T, Q) \leq E_{opt} \quad (12) \]
Algorithm 2: For obtaining the SGN policy parameters: $G_{opt}$, $T_{opt}$ and $Q_{opt}$

1: Begin
2: For $k = 1$ to $M$ do
3: set $W_{min}(k) = 1$;
4: End For
5: For $g = 1$ to $S$ do
6: For $t = 1$ to $S$ do
7: For $q = 1$ to $Q$ do
8: For $m = 1$ to $M$ do
9: $EG_u = 0$;
10: For $i = 0$ to $m$ do
11: $EG_u = EG_u + P_q(i) \times g$;
12: End For
13: $E = EG_u + ES_p$;
14: if $W(t,g,q,m) < W_{min}(k)$ and $E(g,t,q) < E_f$ then
15: $G_{opt} = g$;
16: $T_{opt} = t$;
17: $Q_{opt} = q$;
18: $E_{opt} = E(g,t,q)$;
19: $W_{min}(k) = W(t,g,q,m)$;
20: End if
21: End For
22: End For
23: End For
24: End For
25: End

Thus, the most conservative SGN policy for any $M_0$ is to minimize:

$$G_{opt}, T_{opt}, Q_{opt} = \arg \min_{G,T,Q} (\beta(T, G, Q, M_0))$$  \hspace{1cm} (13)

s.t.

$$E(G, T, Q, M_0) \leq E_{opt}$$  \hspace{1cm} (14)

Finally, the following procedure (cf. Algorithm 2) obtains the SGN policy parameters: $G_{opt}$, $T_{opt}$ and $Q_{opt}$:

5 Illustrative Examples

Figures 3 and 4 present $D_e$ and $E_{Sp}$ after achievement of spotter queries. Figure 3 shows $D_e$ as a function of the number of malicious smart meters varied between 10 and 90 for $N_0 = 100$, and different combinations of
Figure 3  Detection error $\varepsilon_s$ as a function of number of malicious smart meters for $S_0 = 100$ and different $T$ and $Q$.

Figure 4  $E_{Sp}$ as a function of number of malicious smart meters for $S_0 = 100$ and different $T$ and $Q$. 
Figure 5  

\( E \) as a function of number of malicious smart meters for \( S_0 = 100 \) and different \( T, G, \) and \( Q \).

\( T \) and \( Q \). To detect all MSM it is necessary to choose carefully the good combination of \( T \) and \( Q \), i.e. if we choose a small value of \( T \), we must increase the number of sent queries, and otherwise, the \( D_e \) detection error will be remarkable. On the other hand, if we increase \( T \), it will not exceed the number of MSM remaining in the list, otherwise, the probability of detecting all MSM tends to zero, i.e. \( D_e \) will be remarkable too, which explains the great values of \( D_e \) for \( M = 90 \).

We notice that all values of MSM have a combination of \( T \) and \( Q \), which error detection value \( D_e \) tends to zero.

Figure 4 presents expected number of spotter query assignments as a function of malicious smart meters \( M \), \( E_{sp} = T \cdot Q \) always holds for the considered \( T \) and \( Q \) from \( M = 10 \) to \( M = 80 \), because the list contains more smart meters than those are used in any spotter queries. In the case \( M = 90 \), the list of smart meters can contain fewer than \( T \), which explains the decrease of \( E_{sp} \).

Figures 5 and 6 present \( E \) and \( W \) after achievement of genuine query. Figure 5 shows \( E \) as a function of the number of malicious smart meters
varied between 10 and 90 for \( N_0 = 100 \), \( E = T \cdot Q + G \) always holds for the considered \( T, G \) and \( Q \) from \( M = 10 \) to \( M = 80 \), because the list contains more smart meters than those used. In the case \( M = 90 \), the list of smart meters can contain fewer than \( T \) and \( Z \), which explains the decrease of \( E \).

Figure 6 shows \( W \) as a function of the number of malicious smart meters varied between 10 and 90 for \( N_0 = 100 \), all combinations have a value of \( W \) thanks to the null value of \( D_e \) and to a good choice of \( G \). So, if \( D_e \) decreases and \( G \) increases then \( W \) decrease.

Finally, we deduce that in order to obtain a minimum value for all number of malicious smart meters, we must choose carefully the good values of the parameters \( T, G \) and \( Q \).

### 6 Optimal Solutions for the Maximum Value \( E_m \)

In this section we will present the optimization of the parameters \( T, G, Q, E \) and \( W \) as a function of malicious smart meters \( M \) for six values of \( E_m \) in
three cases: \( S_0 = 10 \), \( S_0 = 20 \) and \( S_0 = 50 \), with \( M_0 = S_0 - 2 \) in the three cases.

For different \( E_m \) the optimal solutions behave differently. When \( E_m \) is small, the SGN can afford an increase in the number of spotter queries because \( T \) and \( G \) remain small. With an increase in \( S_0 \), the MSM tries to involve more smart meters into spot-checking, while the overhead constraint limits the number of spotter queries. The complex interaction between all MSM policy parameters makes intuitive choice of their optimal combination impossible and very complex. Thus, the suggested method is necessary to confront the collusive attacks in an efficient manner.

Figures 7–11 present respectively \( T_{opt} \), \( G_{opt} \), \( Q_{opt} \), \( E_{opt} \) and \( W \) as a function of malicious smart meters \( M \) for \( S_0 = 10 \) with different values of \( E_m \).

It can be seen that in five cases of \( E_m \), \( T_{opt} \) decreases with the increase of \( M \), \( Q_{opt} \) increases with the increase of \( M \) and \( G_{opt} \) remains always equal to 1 and \( W \) remains always zero, and we notice that in most cases we can reach a null \( W \) with an \( E_{opt} < E_m \). On the other hand, if \( E_m \) is small, \( E_m = 10 \), we have a disturbance in the results and the increase of the \( G_{opt} \) values.

![Figure 7](image-url)  
**Figure 7** \( T_{opt} \) as a function of number of malicious smart meters for \( S_0 = 10 \) and different \( E_m \).
Figure 8 $G_{opt}$ as a function of number of malicious smart meters for $S_0 = 10$ and different $E_m$.

Figure 9 $Q_{opt}$ as a function of number of malicious smart meters for $S_0 = 10$ and different $E_m$. 
Figure 10 $E_{opt}$ as a function of number of malicious smart meters for $S_0 = 10$ and different $E_m$.

Figure 11 $W$ as a function of number of malicious smart meters for $S_0 = 10$ and different $E_m$. 
between $M = 4$ and $M = 8$ generates an increase in the values of $W$ which reaches up to 0.218. However, the increase of the overhead can again lead to a considerable reduction of $W$, and an analysis of $E_{opt}$ curve allows making the decision about the reasonable overhead level.

Figures 12–16 present respectively $T_{opt}$, $G_{opt}$, $Q_{opt}$, $E_{opt}$ and $W$ as a function of malicious smart meters $M$ for $S_0 = 20$ with different values of $E_m$.

It can be seen that we can divide this case into two, case 1: $W = 0$ and case 2: $W > 0$:

**Case 1:** This case is valid for the values $E_m = 25$, $E_m = 30$ and $E_m = 35$, and $T_{opt}$ decreases with the increase of $M$, $Q_{opt}$ increases with the increase of $M$ and $G_{opt}$ is always equal to 1.

**Case 2:** This case is valid for the values $E_m = 10$, $E_m = 15$ and $E_m = 20$, $T_{opt}$ increases with the increase of $M$, and we notice a disruption to the values of $G_{opt}$ that generates an increase value of $W$ which reaches $W = 0.7$.

![Figure 12](image-url)  
*Figure 12* $T_{opt}$ as a function of number of malicious smart meters for $S_0 = 20$ and different $E_m$. 
Figure 13  $G_{opt}$ as a function of number of malicious smart meters for $S_0 = 20$ and different $E_m$.

Figure 14  $Q_{opt}$ as a function of number of malicious smart meters for $S_0 = 20$ and different $E_m$. 
Figure 15  $E_{\text{opt}}$ as a function of number of malicious smart meters for $S_0 = 20$ and different $E_m$.

Figure 16  $W_{\text{min}}$ as a function of number of malicious smart meters for $S_0 = 20$ and different $E_m$. 
We notice in most cases we can reach a null $W$ with $E_{opt} < E_m$, and the PAWD $W$ is always decreasing because the probability of detecting $MSMs$ by the spotter queries and removing $MSMs$ from the list increases with $E$. On the other hand, it’s clear that with an increase in the number of malicious smart meters, the $SGN$ tends to increase the number of smart meters used for spotter queries and decrease the number of smart meters assigned to the genuine query.

Figures 17–21 present respectively $T_{opt}$, $G_{opt}$, $Q_{opt}$, $E_{opt}$ and $W$ as a function of malicious smart meters $M$ for $S_0 = 50$ with different values of $E_m$.

In this case, when $S_0 = 50$, the number of $MSMs$ can be very high. We can divide it into two cases: case 1: $1 \leq M < 25$ and $25 \leq M \leq 48$:

**Case 1**: $1 \leq M < 25$; in this case, we have a perturbation in the values of $T_{opt}$ and $Q_{opt}$, $G_{opt}$ and $E_{opt}$ increases with the increase of $M$, but $W$ remains almost zero.

![Figure 17](image-url)  
**Figure 17** $T_{opt}$ as a function of number of malicious smart meters for $S_0 = 50$ and different $E_m$. 

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256  
E. Y. Dari et al.
Figure 18  $G_{opt}$ as a function of number of malicious smart meters for $S_0 = 50$ and different $E_m$.

Figure 19  $Q_{opt}$ as a function of number of malicious smart meters for $S_0 = 50$ and different $E_m$. 
Figure 20 \( E_{\text{opt}} \) as a function of number of malicious smart meters for \( S_0 = 50 \) and different \( E_m \).

Figure 21 \( W_{\text{min}} \) as a function of number of malicious smart meters for \( S_0 = 50 \) and different \( E_m \).
Case 2: $25 \leq M \leq 48$: in this case, $Q_{opt}$, $E_{opt}$ and $W$ increases with the increase of $M$, $G_{opt}$ decreases and is fixed in $G = 2$ with the increase of $M$, and $Q_{opt}$ has varied values but with a low thickness.

The best strategy used by $SGN$ is to try to detect all MSMs by sending spotter queries to as many smart meters as possible, reducing the number of smart meters allocated to the genuine query. However, the overhead $E$ increases with the increase of $M$, and the $W$ decreases with the increase of the overhead.

It’s clear that with a reduction in $M_0$ the PAWD $W$ decreases. Indeed, certain knowledge of $M_0$ allows $SGN$ to choose optimal minimizing PAWD for this parameter.

7 Conclusion

Collusion detection and tolerance deserve great research interest from the various distributed computing systems such as smart grid. In this paper, we formulate and solve the spot-checking optimization problem to the collusive behaviour of the smart meters in smart grid.

A repetitive method is proposed, in this work, to measure and evaluate the probability of accepting wrong data (PAWD) and the expected overhead in terms of the total number of query assignments for our system. This method resolves the spot-checking optimization problem by finding the optimal combination of query send policy parameters (the number of deployed spotter queries, the number of smart meters tested by each spotter query, and the number of smart meters for performing the genuine query) minimizing the PAWD while satisfying the expected overhead parameter.

Finally, the obtained results can contribute in optimal distribution and assignment of all components of smart grid system for secure, reliable and cost-aware operation of this system.

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