Transport Theoretical Description of Collisional Energy Loss in Infinite Quark-Gluon Matter

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Abstract. We study the time evolution of a high-momentum gluon or quark propagating through an infinite, thermalized, partonic medium utilizing a Boltzmann equation approach. We calculate the collisional energy loss of the parton, study its temperature and flavor dependence as well as the momentum broadening incurred through multiple interactions. Our transport calculations agree well with analytic calculations of collisional energy-loss where available, but offer the unique opportunity to address the medium response as well in a consistent fashion.

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1. Introduction

The currently prevailing view on the structure of the matter produced in nuclear collisions at the Relativistic Heavy-Ion Collider (RHIC) is anchored by two experimental observations [1, 2, 3, 4, 5]: (1) The emission of hadrons with a transverse momentum $p_T$ of several GeV/c or more is strongly suppressed (jet-quenching), implying the presence of matter of with a very large color opacity, and (2) The anisotropic (“elliptic”) flow in non-central collisions is near the ideal hydrodynamic limit, requiring an early onset of the period during which the expansion is governed by fluid dynamics (earlier than 1 fm/c after the initial impact) as well as nearly ideal fluid properties with a viscosity-to-entropy density ratio $\eta/s \ll 1$. The matter created at RHIC has been thus called the strongly interacting Quark-Gluon Plasma (sQGP) [6].

The origin of the jet-quenching phenomenon can be understood as follows [7]: during the early pre-equilibrium stage of the relativistic heavy-ion collision, scattering of partons causing the formation of deconfined quark-gluon matter often engenders large momentum transfers which leads to the formation of two back-to-back hard partons. These traverse the dense medium, losing energy and finally fragment into hadrons which are observed by the experiments. Within the framework of perturbative QCD, the process with largest energy loss of a fast parton is gluon radiation induced by collisions with the quasi-thermal medium. Elastic collisions add to the energy loss and are thought to be the dominant process for heavy quarks traversing the deconfined medium.

Even though the phenomenon is being referred to as ”jet-quenching”, the overwhelming majority of computations of this effect have focused on the leading particle of the jet and do not take the evolution of the radiated quanta into account. A variety of schemes for quantitative calculations of the radiative energy loss have been developed [8, 9, 10, 11, 12, 13]. However, quantitative comparisons of theoretical model predictions incorporating a realistic hydrodynamic medium evolution with data from relativistic heavy ion collisions at RHIC [14] have revealed significant remaining ambiguities in the value of the extracted transport coefficients of the sQGP [15]. Different leading particle energy loss schemes may thus imply different values for these transport coefficients [7]. A systematic comparison of the assumptions underlying the various leading particle energy loss schemes and of their numerical implementations is currently under way [16, 7].

Recently, with the advent of sophisticated experimental techniques for the reconstruction of full jets emitted from an ultra-relativistic heavy-ion collision [17, 18], attention has shifted from leading particle energy-loss to the evolution of medium-modified jets. The study of the evolution of the entire jet in the medium is expected to lead to a better understanding of the dynamics of energy-deposition into medium and of the subsequent medium response, e.g. the possible formation of Mach-cones etc. [19, 20, 21]. The current state of the art in for medium modified jets are Monte-Carlo generators [22, 23, 24, 25], which calculate the medium-modified jet but do not take the medium response into account. The consistent treatment of the jet in medium as well as the medium response requires the application of transport theory, e.g. via Boltzmann
equation based calculation, such as is done in the Parton Cascade Model (PCM) [26]. Parton Cascades have already been applied to the time-evolution of ultra-relativistic heavy-ion collisions. However, for the most part the PCM calculations have focused on reaction dynamics [27, 28], thermalization [29], electromagnetic probes [30, 31] and bulk properties of the medium [32], as well as to a far lesser extent on leading particle energy-loss [33, 34]. We would also like to note the recent progress in combining a Boltzmann equation based particle transport approach with pQCD cross sections for the scattering of high momentum particles with soft particle interactions mediated by a Yang-Mills field [35].

It is our long-term goal to advance the application of the PCM to the description medium modified jets and the respective response of the medium to a jet propagating through it and depositing energy in it. The achievement of this goal requires the validation of the PCM against analytic test cases which can be reliably calculated for a simplified medium, e.g. a pure gluon plasma or a quark-gluon plasma in thermal and chemical equilibrium. In the present manuscript we take a first step in this direction. We calculate elastic energy loss in an infinite, homogeneous medium at fixed temperature within the PCM approach and compare our results to analytic calculations of the same quantity. In addition, we calculate the rate of momentum broadening of a hard parton propagating through the medium and compare the results of our analysis to analytic expressions for the transport coefficient \( \hat{q} \).

2. Quark Gluon Plasma and Parton Cascade Simulations

The medium in our calculations is an ideal Quark-Gluon-Plasma, i.e. a gas of \( u, d \) and \( s \) quarks and anti-quarks as well as gluons at fixed temperature \( T \) in full thermal and chemical equilibrium. In addition, we also conduct studies for a one-component gluon plasma in thermal and chemical equilibrium. For our transport calculation we define a box with periodic boundary conditions (to simulate infinite matter) and sample thermal quark and gluon distribution functions to generate an ensemble of particles at a given temperature and zero chemical potential. We then insert a hard probe, i.e. a high momentum parton, into the box and track its evolution through the medium. The medium particles may interact with the probe as well as with each other according to a Boltzmann Transport equation:

\[
p' \frac{\partial}{\partial p^\mu} F_i(x, p) = C_i[F] \tag{1}
\]

where the collision term \( C_i \) is a nonlinear functional of the phase-space distribution function. Although the collision term, in principle, includes factors encoding the Bose-Einstein or Fermi-Dirac statistics of the partons, we neglect those effects here.

The collision integrals have the form:

\[
C_i[F] = \frac{(2\pi)^4}{2S_iE_i} \cdot \int \prod_j d\Gamma_j |\mathcal{M}|^2 \delta^4(P_{in} - P_{out}) D(F_k(x, p)) \tag{2}
\]
with
\[ D(F_k(x, \vec{p})) = \prod_{\text{out}} F_k(x, \vec{p}) - \prod_{\text{in}} F_k(x, \vec{p}) \] (3)
and
\[ \prod_j d\Gamma_j = \prod_{j \neq i} \frac{d^3p_j}{(2\pi)^3 (2p_j^0)} . \] (4)

\( S_i \) is a statistical factor defined as
\[ S_i = \prod_{j \neq i} K_{a!}^{\text{in}} K_{a!}^{\text{out}} \] with \( K_{a!}^{\text{in, out}} \) identical partons of species \( a \) in the initial or final state of the process, excluding the \( i \)th parton.

The matrix elements \(|M|^2\) account for the following processes:
\[
\begin{align*}
&gg \to gg & qq \to qq & gg \to gg \\
&qq' \to qq' & qq \to \bar{q}q & gg \to \bar{g}g \\
&(gg \to q\bar{q}) & (q\bar{q} \to gg) & (q\bar{q} \to q'\bar{q}')
\end{align*}
\] (5)

with \( q \) and \( q' \) denoting different quark flavors. The flavor changing processes in parenthesis are optional and can be disabled to study the effect of jet flavor conversion. The gluon radiation processes, e.g. \( gg \to ggg \) are not included in this study, but will be addressed in a forthcoming publication. The amplitudes for the above processes have been calculated in refs. [36, 37] for massless quarks. The corresponding scattering cross sections are expressed in terms of spin- and colour-averaged amplitudes \(|M|^2\):
\[
\left( \frac{d\hat{\sigma}}{dQ^2} \right)_{ab \to cd} = \frac{1}{16\pi s^2} \langle |M|^2 \rangle
\] (6)

For the transport calculation we also need the total cross section as a function of \( \hat{s} \) which can be obtained from (6):
\[
\hat{\sigma}_{ab}(\hat{s}) = \sum_{c,d} \int_{(p_T^{\text{min}})^2}^{\hat{s}} \left( \frac{d\hat{\sigma}}{dQ^2} \right)_{ab \to cd} dQ^2 .
\] (7)

Since our medium is in full thermal and chemical equilibrium, we can use the effective thermal mass of a gluon and a quark in the system to regularize the cross sections [38]:
\[
\mu_D^2 = \pi \alpha_s d_p \int \frac{d^3p}{(2\pi)^3} \frac{C_2}{|\vec{p}|} f_p(\vec{p}; T),
\] (8)

where \( d_p \) is the degeneracy factor of a parton \( p \) and \( C_2 \) is \( N_c \) for gluons and \((N_c^2 - 1)/(2N_c)\) for quarks. Inserting the thermal distribution yields a Debye mass of a gluon of \( \mu_D = gT \) in a thermal gluon system at temperature \( T \) and of \( \mu_D = \sqrt{(2N_c + N_f)/6gT} \) for quarks and gluons in a quark-gluon plasma. For example, the dominant elastic cross sections thus are:
\[
\begin{align*}
\frac{d\sigma_{gg \to gg}}{dq^2} &= 2\pi \alpha_s^2 \frac{9}{4} \frac{1}{(q^2 + \mu_D^2)^2}, \\
\frac{d\sigma_{gg \to gq}}{dq^2} &= 2\pi \alpha_s^2 \frac{1}{(q^2 + \mu_D^2)^2}, \\
\frac{d\sigma_{gq \to gq}}{dq^2} &= 2\pi \alpha_s^2 \frac{4}{9} \frac{1}{(q^2 + \mu_D^2)^2},
\end{align*}
\] (9-11)
where the first order of Feynman diagrams have been included.

For our studies we use two distinct implementations of the Parton Cascade Model, the the Andong parton cascade code [39], and the VNI/BMS code [28]. Both codes have been modified to contain the same cross sections so that we can verify the outcome of our calculations through cross-comparisons between the two PCM implementations. For the sake of simplicity we keep the coupling constant fixed at a value of $\alpha_s = 0.3$.

To obtain the temporal evolution of a high momentum parton propagating through a gluon or a quark-gluon plasma, a high energy gluon or quark of initial energy $E_0$ is injected into or thermal (quark-)gluon-plasma box at the center of it’s xy-plane with $\vec{p} = (0, 0, p_z = \sqrt{E_0^2})$. Following each individual scattering event involving our hard probe, we record the energies and momenta of the outgoing partons. The parton with the larger momentum in the final state is considered to be our continuing probe particle, due to the dominance of small angle scattering in the implemented cross sections. A simple estimate on the number of interactions the probe will undergo per unit time or length can be obtained via its mean free path in the medium:

$$\lambda_s = \frac{1}{\sigma_T \rho},$$

(12)

where $\sigma_T$ is the total thermal cross section and $\rho$ the density of a medium. A gluon’s mean free path in a gluon plasma is 1.1 fm at $T = 300$ MeV and 0.76 fm at $T = 400$ MeV, and in the quark-gluon plasma 0.83 fm and 0.59 fm, respectively. The quark mean free paths are about 9/4 times longer than those of gluon ones at same temperature.

3. Results and Discussion

In our work, we shall focus solely on the hard parton propagating through the medium and analyze its energy loss and momentum broadening as a function of time and distance traveled. We would like to point out that our calculation includes the full information on the medium-response as well, however, a detailed analysis on its characteristics it outside the scope of the present work and will be discussed in a forthcoming publication.

Let us start by comparing the distribution of transverse momentum transfers experienced by gluons with $E_0 = 100$ GeV and $E_0 = 500$ GeV, respectively, while propagating through a gluon plasma at $T = 300$ MeV to the analytic expression given by the differential cross section [11].

Figure 1 shows that we find excellent agreement between our transport calculation and the analytic expression for $E_0 = 500$ GeV. At the lower incident probe energy, $E_0 = 100$ GeV we note a suppression in the high momentum transfer tail of the distribution which we can attribute to the effects of phase space and energy conservation, the gluon loses a substantial amount of energy while traversing a medium of 50 fm depth and thus for most of the time does not carry sufficient momentum to scatter with high momentum transfers while the analytic formula continuously assumes that the CM energy between the colliding particles is much larger than the Debye mass.
We now focus on the elastic energy loss of a high-momentum parton in medium. The left frame of Fig. 2 shows the energy as a function of time for a gluon with initial energy of 100 GeV (or 50 GeV, respectively), propagating through a quark-gluon plasma (QGP) or gluon plasma (GP) at a temperature of $T=400$ MeV. The right frame repeats the calculation for a light quark instead of a gluon. The calculation, which includes only elastic processes (i.e. the flavor exchange reaction channels have been disabled in order to unambiguously study the flavor dependence) clearly shows the anticipated linear decrease of jet energy with time. One should note, that analytic calculations usually study the jet energy as a function of distance traveled – in our case we substitute time for distance in order to have a quantity that is not affected by the periodic boundary conditions for the system in our calculations. We have verified the linear relationship between distance traveled and elapsed time with a slope near unity.

The two frames clearly show the difference between a GP and a QGP in terms of energy-loss at the same temperature. This difference is due to the significantly higher parton density in a QGP compared with a GP for the same temperature, resulting in a larger number of scattering partners for the hard probe to interact with. The difference

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure1.png}
\caption{The Monte Carlo sampling of transverse momentum transfer at each scattering. The jet only is allowed to have a collision with medium particles.}
\end{figure}
Figure 2. Left: the gluon jet energy as a function of traveling time in the medium at $T = 400\,\text{MeV}$: The travelling distance is proportional to the time. GP is a gluon plasma and QGP a quark-gluon plasma and the simulation does not include $gg \rightarrow ggg$ process. Right: the quark jet energy as a function of time: The penetration length is proportional to the time. Plasma temperature $T = 400\,\text{MeV}$.

Figure 3. Left: gluon energy as a function of time for different initial values of the energy in a gluon plasma. Right: the same for a fixed initial energy and various medium temperatures. The solid lines represent an analytical calculation (see text for details).

is less pronounced for the quark probe than the gluon probe, due to the difference in their interaction cross sections. We also observe that the linear decrease of energy as a function of time tapers off in the long time limit as the probe energy approaches the thermal regime. While at the probe energies studied here (between 50 GeV and 400 GeV) this occurs at times not relevant in the context of an ultra-relativistic heavy-ion collision, for smaller probe energies frequently seen at RHIC, this may be a significant effect.

Fig. 3 shows the energy and temperature dependence of the elastic energy loss of a hard gluon in a gluon plasma. The calculations (symbols) are compared to an analytical...
Figure 4. Left: Energy as a function of distance for a gluon propagating through a GP and a QGP at the same temperature and at equivalent entropy-densities. A scaling of the energy-loss with the entropy-density is observed. Right: distribution of probe energies after traversing the medium for 5, 10, 50, 70 and 100 fm at a temperature of 300 MeV.

calculation \[40, 41\]:

\[-\frac{dE}{dt} = \int \frac{d^3k}{(2\pi)^3} F_g(\vec{k}; T) \int dq_\perp^2 (1 - \cos \theta) \nu \frac{d\sigma}{dq_\perp^2} \tag{13}\]

where \(\nu = E - E'\) is the energy difference between before and after collision. Utilizing the characteristics of our medium and the cross sections in our calculation, this equation can be discretized to a form which lends itself to a comparison with our calculation:

\[E_p(z) = E_p(0) - z \frac{\alpha_s C_2 \mu_D^2}{2} \ln \left[ \frac{\sqrt{E_p(z)T}}{\mu_D} \right] \tag{14}\]

Using an iterative procedure we can calculate \(E_p(z)\) for the initial gluon energies and temperatures used in Fig. 3 and compare them to our calculation. The agreement between the analytical calculation and the PCM is remarkable and serves as validation of the PCM framework. The validation of the PCM calculation in a well-controlled infinite matter calculation in full equilibrium at fixed temperature is of significant importance, since the PCM can easily be used to study realistic dynamic systems far off equilibrium, e.g. an ultra-relativistic heavy-ion collision, which can only be poorly described in the framework of (semi-)analytic calculations.

In Fig. 2 we observe a difference in the energy loss a parton suffers when propagating through a GP or a QGP. We understand this difference to be due to the different overall particle densities associated with a GP and a QGP at the same temperature. In order to validate this point, we initialized a GP and a QGP at an identical entropy density of \(s = 87.5 \text{ fm}^{-3}\), corresponding to a temperature of \(T = 457\) MeV for a GP and \(T = 318\) MeV for a QGP. The results of this calculation (also in comparison to a GP and a QGP at a temperature of \(T = 400\) MeV) are shown in
Fig. 4 for the same entropy density, both the GP and the QGP inflict a nearly identical amount of elastic energy loss to the hard probe. This scaling suggests that the entropy density, rather than the temperature, may be a robust quantity for the characterization of a thermal QCD medium by energy-loss measurements. We note that it is by no means clear whether the deconfined medium in the early stages of a heavy-ion reaction more closely resembles a GP (or a liberated “glasma” [42]) or a QGP in full chemical equilibrium [38]. Most likely the chemical composition of the deconfined medium created in a ultra-relativistic heavy-ion collision changes significantly as a function of time, whereas its entropy density (after the initial equilibration) does not vary as much.

The right frame of Fig. 4 shows the distribution of probe energies for a gluon with initial energy of 50 GeV passing through a gluon plasma at temperature $T = 300$ MeV after 5, 10, 50, 70 and 100 fm, respectively. The gluon distribution at $t = 0$ is a $\delta$-function at $E = E_0$. The Figure shows several interesting features. We find that elastic energy loss acts as a diffusion processes in momentum space, with the width of the distribution being a function of the traveling distance. Likewise the peak of the distribution shifts as a function of traveling distance. Even after traveling significant distances, about an order of magnitude larger than possible in a relativistic heavy-ion collision, the gluon has not thermalized with the medium, in which a medium particle has an average energy of about 0.9 GeV at $T=300$ MeV.

Another important quantity for the characterization of the hot and dense QCD medium is the transport coefficient $\hat{q}$, which is defined as [43]:

$$\hat{q} = \rho(T) \int dq_\perp^2 q^2 \frac{d\sigma}{dq_\perp^2}$$

with the squared momentum transfer $q^2 = -t$. Generally, $\hat{q}$ can be interpreted as the amount of squared transverse momentum per unit length a probe accumulates as it propagates through the QCD medium. This interpretation lends itself to a definition of $\hat{q}$ suitable for extraction from microscopic transport calculations:

$$\hat{q} = \frac{1}{l_z} \sum_{i=1}^{N_{coll}} (\Delta p_{\perp,i})^2$$

One should note that $\hat{q}$ in general should depend on the distance $l_z$ the probe has traveled through the medium, since the probe loses energy in the process, and thus the average momentum transfers in individual interactions of the probe with the medium may vary as a function of that distance.

Figure 5 shows $\hat{q}$ for a gluon plasma as a function of distance traveled through the medium for several temperatures. The initial values of $\hat{q}$ depend strongly on the temperature, ranging from approximately 1.5 GeV$^2$/fm at $T = 300$ MeV up to about 9 GeV$^2$/fm at 600 MeV temperature. For $T = 400$ MeV we find good agreement with recent calculations by [35] using a Boltzmann transport for hard binary collisions combined with soft interactions mediated by a collective Yang-Mills field and by [34] with the BAMPS parton cascade model in its binary scattering mode. At leading-log
order and in the weak coupling limit, using the same matrix element as in our PCM calculation, the following analytic expression has been derived for $\hat{q}$ [14]:

$$
\hat{q}(\Lambda) \approx \alpha_s T m_D^2 \ln \left( \frac{T^2}{m_D^2} \right) + 4\pi \alpha_s^2 \mathcal{N} \ln \left( \frac{\Lambda^2}{T^2} \right)
$$

(17)

if the cut-off $\Lambda \geq T$. Comparing expression (17) to expression (14) and following the derivation of (17) we find that the cut-off $\Lambda^2 \sim E_p T$. Replacing $\Lambda^2$ by $aE_p(z)T$ (with $a$ being a proportionality constant to be determined) in expression (17) provides a good fit to our results for a choice of $a = 0.1$.

4. Conclusions

We have studied elastic energy loss of high energy parton in an infinite, homogeneous, thermal medium within the PCM approach and have compared our results to analytic calculations of the same quantity. In addition, we have calculated the rate of momentum broadening of a hard parton propagating through the medium and have compared the results of our analysis to an analytic expression for the transport coefficient $\hat{q}$. We find good agreement between the PCM calculations and the analytic expressions (within the approximations used in both cases), giving us significant confidence that our transport approach provides a reliable description of a gas of quarks and gluons at temperatures above $\approx 2T_C$ in the weak coupling limit. We expect that the results presented in this
manuscript can be used as a benchmark by other parton-based microscopic transport calculations. The validation of the PCM against the analytic test cases presented in this manuscript now allows us to advance the application of the PCM to the description of medium modified jets in relativistic heavy-ion collisions and the response of the medium to a hard parton propagating through it.

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