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Hot pixel contamination in the CMB correlation function?

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Abstract. Recently, it was suggested that the map-making procedure, which is applied to the time-ordered CMB data by the WMAP team, might be flawed by hot pixels. This could lead to a bias in the pixels having an angular distance of about $141^\circ$ from hot pixels due to the differential measuring process of the satellite WMAP. Here, the bias is confirmed, and the temperature two-point correlation function $C(\vartheta)$ is reevaluated by excluding the affected pixels. It is shown that the most significant effect occurs in $C(\vartheta)$ at the largest angles near $\vartheta = 180^\circ$. Furthermore, the corrected correlation function $C(\vartheta)$ is applied to the cubic topology of the Universe, and it is found that such a multi-connected universe matches the temperature correlation better than the $\Lambda$CDM concordance model, provided the cubic length scale is close to $L = 4$ measured in units of the Hubble length.

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1. Introduction

One of the most important observational inputs of modern cosmology is provided by the cosmic microwave background (CMB). The sky maps produced by the WMAP team [1] have found wide applications in cosmological parameter extraction and provided several surprises. Besides the low power at large scales, which had already been discovered by COBE [2], some strange properties emerged concerning the statistical isotropy, i.e. an anomalous alignment between the quadrupole and the octopole [3, 4] as well as an asymmetry of the CMB fluctuations within the two hemispheres with respect to the ecliptic plane [5]. Both anomalies are difficult to reconcile within the standard inflationary framework. A possible explanation could be related to the uncertainties which inevitably arise in the foreground removal procedures [6].

Recently, Liu and Li [7, 8] have discussed a possible systematics which lies at the heart of the map-making procedure. The main point arises from the fact that WMAP measures temperature differences at two points on the sphere separated by about $141^\circ$ which is due to the construction of the probe. They demonstrate in [7, 8] that the pixels, which lie on a scan ring having diameter $141^\circ$ with a hot pixel at its centre, systematically obtain a lower temperature. They show that the corresponding cross-correlation function displays a negative correlation at the crucial angle of $141^\circ$ in the
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| channel | Q1, Q2 | V1, V2 | W1, W4 | W2, W3 |
|---------|--------|--------|--------|--------|
| diameter | 144.3° | 140.5° | 139.8° | 142.0° |

Table 1. The diameters of the scan rings in dependence on the channels [9].

three frequency bands Q, V, and W thus pointing to a systematic distortion occurring in all three bands. In order to estimate the magnitude of the induced temperature distortion, they [7, 8] select the 2000 hottest pixels for a detailed analysis and find a temperature distortion in the range between 11μK and 14μK which in turn translates into a 10% difference in the quadrupole and the octopole moments. This systematics is not remedied by a prolonged observation time. It should be noted, however, that the WMAP team [1] computes the average temperature of pixels, which do not belong to the set of hot pixels, by omitting the hot pixels using the processing mask, so that it is not clear at which point of the map-making pipeline this systematics arises. Furthermore, there are no analogous cold pixels since the additional foreground emission always leads to an increase of the measured temperature.

In this paper, we construct a modified mask in order to check whether the suggested systematics really exists. Furthermore, the two-point temperature correlation function $C(\vartheta)$ is investigated with respect to this systematics. With the temperature correlation function, which is based only on those pixels that are not strongly affected by this systematics, we carry out a test of a cubic topology of our Universe.

2. A modified Liu-Li mask

The hot pixel systematics does not affect all pixels on the corresponding scan rings in the same way. To each hot pixel belongs a well defined scan ring, of course, but due to the large number of hot pixels there is an equally large number of affected scan rings, which intersect each other, in general. This is due to the large size of the scan rings having diameters between 135° and 144° depending on the channel [9], see Table 1 for the individual values. Since the suggested systematics leads to a negative bias on a given scan ring, the bias should be more pronounced at the intersections of several affected scan rings. In order to test this effect, a modified Liu-Li mask is constructed by the following procedure.

We start with the five-year Q1, Q2, V1, V2, W1, W2, W3, W4 channel sky maps which are not foreground reduced and thus contain the hot pixels. These maps as well as the KQ75 and KQ85 masks are provided by the WMAP team [1] on the LAMBDA home page lambda.gsfc.nasa.gov. Then all pixels above a given temperature threshold $T_{\text{thres}}$ are selected as hot pixels and their corresponding scan rings with the diameters given in Table 1 are computed. In this way 8 maps are obtained whose pixel values contain the number $N_{\text{inter}}$ of corresponding hot pixels. From these 8 maps we compute 3 average maps, one for each of the three bands Q, V, and W with a mean $N_{\text{inter}}$. If a given pixel obtains more than $N_{\text{inter}}$ intersections from affected scan rings, it gets masked out. This
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Figure 1. The distribution of the CMB temperature values $\delta T$ in $\mu K$ is shown for the ILC (5yr) map by taking into account only the pixels outside the KQ75 mask. The temperature distribution has a standard deviation of 66$\mu K$.

Figure 2. The degree of the disturbance by hot pixels is shown for the threshold $T_{\text{thres}} = 1000\mu K$ in Galactic coordinates. The pixels are represented in dependence on the number $N_{\text{inter}}$ of scan rings with respect to the W band belonging to hot pixels with $\delta T > T_{\text{thres}}$ up to $N_{\text{inter}} = 300$ (colour online).

The value of the temperature threshold $T_{\text{thres}}$ is chosen to be many times larger than the typical temperature fluctuation of the cosmological signal. In Figure 1 the distribution of the temperature values $\delta T$ is shown for the ILC map based on the five-year data [1] by taking into account only the pixels outside the KQ75 mask. The temperature distribution has a standard deviation of 66$\mu K$. We choose in the following three thresholds of 1000$\mu K$, 2000$\mu K$, and 4000$\mu K$, respectively, which are very large compared to the standard deviation of 66$\mu K$ of the CMB signal. In Figure 2 we show the distribution of the affected pixels for the W band for a hot pixel threshold of $T_{\text{thres}} = 1000\mu K$, where the Mollweide projection is used in Galactic coordinates. The intensity of the pixels depends on the number $N_{\text{inter}}$ of hits by scan rings of hot pixels. The scale is truncated at $N_{\text{inter}} = 300$. One observes that the most critical pixels mask depends then on both thresholds $T_{\text{thres}}$ and $N_{\text{inter}}$. In a last step all pixels within the KQ75 or KQ85 mask are rejected. The remaining pixels should be those being less affected by foregrounds and therefore containing the safest cosmological information.
lie below and above the Galactic plane opposite to the Galactic centre which is in the centre of Figure 2. This behaviour is caused by the large diameter of $\sim 141^\circ$ of the scan rings and the fact that many hot pixels above $T_{\text{thres}}$ are near the Galactic centre. The modulus of Galactic latitude of the domain with the largest values of $N_{\text{inter}}$ is given by $180^\circ - 141^\circ = 39^\circ$ revealed by the dark regions in Figure 2.

An alternative point of view is to consider the magnitude of foreground which is related to a given pixel without using any thresholds. For each pixel we compute the average of the temperatures of all those pixels having a distance of $141^\circ$ from the considered one. Since such a $141^\circ$ ring contains a large number of pixels, the CMB signal as well as noise will cancel in the average. The average of these temperatures is thus a measure of the amount of foreground which can influence the accuracy of the determination of the temperature. The sky map shown in Figure 3 displays this temperature average. The comparison with Figure 2 clearly shows that the same areas on the sky are affected.

In order to verify the negative-temperature bias of the pixels belonging to hot pixel scan rings, the mean temperature $\delta T_{\text{mean}}$ and the corresponding noise are computed inside the modified Liu-Li mask with $T_{\text{thres}} = 1000 \mu K$ but outside the KQ75 mask. The mean $\delta T_{\text{mean}}$ depends on the chosen value of the threshold number $N_{\text{inter}}$, i.e. pixels are selected if they are related to at least $N_{\text{inter}}$ hot pixels. This procedure tests whether the negative bias increases with the number $N_{\text{inter}}$ of scan rings. Figure 4a reveals that $\delta T_{\text{mean}}$ computed for the W band foreground-reduced map indeed drops towards more negative values until a value of $N_{\text{inter}} \sim 140$ is reached. The pixels with $N_{\text{inter}} \gtrsim 140$ possess a temperature bias of the order of $-25 \mu K$. This is the expected behaviour since with increasing $N_{\text{inter}}$ only the most severely affected pixels are taken into account, i.e. those with the largest systematics. Whereas panel a) displays $\delta T_{\text{mean}}$ computed from those pixels having at least $N_{\text{inter}}$ hot pixels, panel b) shows the mean value $\delta T_{\text{inter}}$ computed only from those pixels having exactly $N_{\text{inter}}$ hot pixels. The number of the latter ones is lower and thus the curve possesses larger statistical fluctuations. But it nevertheless demonstrates the negative bias for pixels with $N_{\text{inter}}$ above 100.
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Figure 4. The mean temperature $\delta T_{\text{mean}}$ is shown for the W band foreground-reduced map (5yr). The mean value is computed from the pixels inside the modified Liu-Li mask for the W band with $T_{\text{thres}} = 1000$ $\mu$K but outside the KQ75 mask in dependence on the threshold $N_{\text{inter}}$. In Panel a) the value of $\delta T_{\text{mean}}$ is computed from those pixels which are related to at least $N_{\text{inter}}$ hot pixels. The grey band represents the $2\sigma$ uncertainty of the detector noise in the corresponding area. The shaded region denotes the $2\sigma$ uncertainty obtained from 100,000 simulations of $\Lambda$CDM models subjected to the same procedure. The dotted curves show the $3\sigma$ uncertainties. In Panel b) the mean temperature $\delta T_{\text{inter}}$ is computed from pixels corresponding to exactly $N_{\text{inter}}$ hot pixels.

In order to check the significance of this result, 100,000 simulations of $\Lambda$CDM concordance models are generated for which $\delta T_{\text{mean}}$ is computed using the same procedure as outlined above. These values scatter symmetrically around a zero mean. The shaded region in Figure 4a denotes the $2\sigma$ deviation from the zero mean. One observes that the W band distortion is over a wide range of values of $N_{\text{inter}}$ larger than the $2\sigma$ deviation for $\Lambda$CDM models. This demonstrates that there is a systematics for these pixels.

Figures 5 and 6 present the result of the same analysis as shown in Figure 4, but for the V and Q bands, respectively. In both frequency bands the same negative bias of at least $2\sigma$ is observed when $N_{\text{inter}}$ is sufficiently large, i.e. when enough hot pixels are connected to the considered one. For very large values of $N_{\text{inter}}$ the deviation is smaller than $2\sigma$ but very few pixels occur in that range. The values of $N_{\text{inter}}$ cannot be directly compared between the different channels since they possess different hot
pixels lying above $T_{\text{thres}}$ because of the different foregrounds. In the case of the W band the dust contribution dominates whereas the synchrotron and free-free emission is more important in the case of the V and Q bands.

None of our 100 000 simulations of ΛCDM concordance models yields a $\delta T_{\text{mean}}$ curve which always has values below the WMAP result shown in the panel a) of Figures 4 - 6. The same result is obtained for $\delta T_{\text{inter}}$ shown in the corresponding panel b). This emphasizes the peculiarity of the negative-temperature bias.

3. The correlation hole at $\vartheta = 180^\circ$

Let us now come to the temperature two-point correlation function $C(\vartheta)$, which is defined as

$$C(\vartheta) := \langle \delta T(\hat{n})\delta T(\hat{n}') \rangle \quad \text{with} \quad \hat{n} \cdot \hat{n}' = \cos \vartheta \ .$$  (1)

It was computed by [2] from the COBE 4yr data and was found to display unexpectedly low power at large angles $\vartheta \gtrsim 60^\circ$. At these large angles $C(\vartheta)$ is close to zero. Only near $\vartheta = 180^\circ$ it shows a slight negative power, which is much more pronounced in the WMAP five-year data [10]. This anticorrelation of antipodal points is the so-called "correlation hole". Copi et al. [10] show the strong dependence of the correlation hole on the chosen mask. The correlation function $C(\vartheta)$ possesses the largest antipodal

Figure 5. As in Figure 4 the mean temperatures $\delta T_{\text{mean}}$ and $\delta T_{\text{inter}}$ are shown but for the V band foreground-reduced map (5yr).
anticorrelation if one uses no mask at all, whereas applying the KQ75 mask reduces
the anticorrelation, but it is nevertheless present. They conclude that the full-sky
results seem inconsistent with the cut-sky results. Furthermore, most of the large-angle
correlation in reconstructed sky maps lies inside the part of the sky that is contaminated
by the Galaxy.

We do not take into account the cosmic variance which arises on the theoretical
side since the cosmic initial conditions are assumed only on statistical grounds. Here,
we are interested in the correlation function \( C(\vartheta) \) observed from our special observer
point within our Universe.

We now show that the remaining negative correlation near \( \vartheta = 180^\circ \) is caused by the
pixels lying within the modified Liu-Li mask. To that aim we apply our modified Liu-Li
mask with \( T_{\text{thres}} = 1000 \mu K \) together with the KQ75 mask to the W band foreground-
reduced map (5yr) for several choices of the intersection threshold \( N_{\text{inter}} \). The result
shown in Figure 7 reveals a pronounced correlation hole for large values of \( N_{\text{inter}} \), i.e.
for those cases where only a small number of further pixels is rejected after applying
the KQ75 mask. The curve belonging to \( N_{\text{inter}} = 200 \) displays almost the usual result
obtained by using only the KQ75 mask, whereas the one belonging to \( N_{\text{inter}} = 60 \) shows
even positive correlations near \( \vartheta = 180^\circ \). The four cases presented in Figure 7 also
demonstrate that the correlation is at other angular separations \( \vartheta \) nearly independent
Figure 7. The correlation function $C(\vartheta)$ is computed from the W band foreground-reduced map (5yr) using the pixels outside the KQ75 mask. In addition the pixels inside the modified Liu-Li mask are rejected for 4 different values of the threshold $N_{\text{inter}}$. The remaining pixels correspond to 69.9%, 64.1%, 61.1%, and 57.3% of the full sky for $N_{\text{inter}} = 200$, 100, 80, and 60, respectively.

Figure 8. As in Figure 7 the correlation function $C(\vartheta)$ is computed using the pixels outside the KQ75 mask but now for the ILC map (5yr). Again the pixels inside the modified Liu-Li mask are rejected for 4 different values of the threshold $N_{\text{inter}}$.

on the value $N_{\text{inter}}$ except for the interval $[30^\circ, 50^\circ]$. However, the strongest sensitivity occurs at $\vartheta = 180^\circ$. At present, one cannot decide the important question which value of $N_{\text{inter}}$ would be optimal or the most probable one. The answer will be given by future measurements.

Figure 8 shows a second evaluation but instead of the W band foreground-reduced map, the ILC (5yr) map is used. The comparison of both figures reveals that there are no significant differences such that the hot pixel systematics propagates from the individual band maps to the final ILC map.

Let us now address the question how probable such a behaviour is with respect to the $\Lambda$CDM concordance model. In order to compute the probability that $C(\vartheta)$ remains
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Inter = 200
Inter = 150
Inter = 100
Inter = 80
Inter = 60

2 4 6 8 10 12 14 16 18 20

0 250 500 750 1000 1250 1500

Figure 9. The angular power spectrum $\delta T^2_l$ is estimated from the correlation function $C(\vartheta)$ based on the W band foreground-reduced map (5yr) using the pixels outside the KQ75 mask. In addition the pixels inside the modified Liu-Li mask are rejected for 4 different values of the threshold $N_{\text{inter}}$. The $\delta T^2_l$ values obtained by the WMAP team are shown as open circles [11].

nearly unchanged for $50^\circ < \vartheta < 165^\circ$, define the difference

$$\Delta C(\vartheta) := C_{\text{KQ75+LL}}(\vartheta) - C_{\text{KQ75}}(\vartheta)$$

between $C(\vartheta)$ using the KQ75 mask and the modified Liu-Li mask for $N_{\text{inter}} = 60$, which is denoted as $C_{\text{KQ75+LL}}(\vartheta)$, and $C(\vartheta)$ using only the KQ75 mask denoted as $C_{\text{KQ75}}(\vartheta)$. The integrated quantity

$$D := \int_{\vartheta=50^\circ}^{\vartheta=165^\circ} d \vartheta |\Delta C(\vartheta)|$$

measures how strongly $C(\vartheta)$ is affected by the suspected pixels. The value obtained from the W band data is surprisingly low, indeed from our 100 000 $\Lambda$CDM concordance models only 495 models possess a smaller value, i.e. $D_{\Lambda\text{CDM}} < D_{\text{WMAP}}$. Thus, 99.5% of the $\Lambda$CDM models show a stronger change in $C(\vartheta)$ than the considered WMAP data. Concerning the correlation hole, only 3111 models satisfy $\Delta C_{\Lambda\text{CDM}}(180^\circ) > \Delta C_{\text{WMAP}}(180^\circ)$, i.e. the large increase of $C(\vartheta)$ at $\vartheta = 180^\circ$ is also unusual at the 3 percent level. If one requires both conditions simultaneously not a single $\Lambda$CDM model remains. This emphasizes the unusual behaviour of the suspected pixels.

Although we emphasized up to now the correlation function $C(\vartheta)$, it is instructive to study also the effect of the hot pixels on the angular power spectrum $\delta T^2_l$. To that aim we use the integral transform of the correlation function $C(\vartheta)$ computed above in order to obtain an estimation of the angular power spectrum $\delta T^2_l$. The result is shown in Figure 9 with respect to the W band and in Figure 10 with respect to the ILC map and is also given in Table 2. Due to the minute differences in $C(\vartheta)$ with respect to the W band map and the ILC map, the differences in $\delta T^2_l$ are also very small for these two cases. The comparison with the 5yr values of $\delta T^2_l$ obtained by the WMAP team [11] shows that the power $\delta T^2_l$ obtained from domains not masked by the modified Liu-Li masks tends to result in lower values than those of the WMAP team for $l < 8$. In contrast to the values
Figure 10. As in Figure 9 an estimation of the angular power spectrum $\delta T^2_l$ is shown but now using the ILC map (5yr). The $\delta T^2_l$ values obtained by the WMAP team are shown as open circles [11].

| multipole | $l = 2$ | $l = 3$ | $l = 4$ | $l = 5$ |
|-----------|---------|---------|---------|---------|
| W band, $N_{\text{inter}} = 200$ | 79  | 336  | 738  | 1168  |
| W band, $N_{\text{inter}} = 100$ | 98  | 314  | 651  | 1023  |
| W band, $N_{\text{inter}} = 80$ | 118 | 296  | 642  | 939   |
| W band, $N_{\text{inter}} = 60$ | 152 | 260  | 679  | 873   |
| ILC, $N_{\text{inter}} = 200$ | 94  | 320  | 728  | 1134  |
| ILC, $N_{\text{inter}} = 100$ | 107 | 311  | 665  | 984   |
| ILC, $N_{\text{inter}} = 80$  | 128 | 292  | 662  | 898   |
| ILC, $N_{\text{inter}} = 60$  | 164 | 259  | 721  | 836   |

Table 2. The values for the angular power spectrum $\delta T^2_l$ in dependence on the four masks used in Figure 7. The spectrum is given in units of $\mu K^2$.

of the WMAP team, the power $\delta T^2_l$ increases monotonically from $l = 2$ up to $l = 5$ by using only pixels not affected by the masks.

4. The cubic topology for the modified correlation function

The surprisingly low CMB large-angle power of the correlation function $C(\vartheta)$, which was discovered in [2], is at variance with the $\Lambda$CDM concordance model as has been found in [12] and recently emphasized in [13] and [10]. One of the possible explanations for this unexpected behaviour is provided by models of the Universe whose spatial section is represented by a multi-connected space form. For a general introduction to the topology with respect to cosmology, see e.g. [14, 15, 16, 17, 18, 19]. In these models exists naturally a largest wavelength at which perturbations can occur as seeds for structure formation. This wavelength is mainly determined by the size of the topological space form. The correlation function $C(\vartheta)$ has been studied for several multi-connected space forms, and a low large-angle power has been shown to exist in the case of the hyperbolic
Picard topology [20, 21], the spherical Poincaré dodecahedron [22], and the flat toroidal universe [13].

In [13] we have analysed the WMAP three-year data with respect to the question whether a flat toroidal universe, i.e. a cubic topology, is compatible with the CMB observations. To that aim the correlation function $C_{\text{model}}(\vartheta)$ obtained from the cubic topology with side length $L$ is compared to the observed correlation function $C_{\text{obs}}(\vartheta)$ by using the integrated weighted temperature correlation difference

$$I := \int_{-1}^{1} d\cos \vartheta \frac{(C_{\text{model}}(\vartheta) - C_{\text{obs}}(\vartheta))^2}{\text{Var}(C_{\text{model}}(\vartheta))}.$$  

(4)

It is found in [13] that the results depend on the chosen mask that is applied to the CMB data. Applying the kp0 mask to the data shows that cubic topologies around $L = 3.86$ are preferred whereas using no mask at all leads to models having a size around $L = 4.35$. ($L$ is given in units of the Hubble length $L_H = c/H_0 \simeq 4.26\text{Gpc}$ for $h = 0.704$.) This demonstrates the sensitivity on the pixels that are selected for the computation of the correlation function $C(\vartheta)$.

Instead of using the three-year data as in [13], we now compute the measure $I(L)$, eq. (4), using the updated five-year data, where we use the W band foreground reduced map. The analysis is now restricted to the W band since, as shown in the previous section, the results for the ILC map are nearly identical. Furthermore, we apply the KQ75 mask together with the four modified Liu-Li masks discussed above. The result shown in Figure 11 is that cubic topologies slightly smaller than $L = 4$ lead to the smallest values of $I(L)$, i.e. lead to the best agreement with the data. The corresponding values for the $\Lambda$CDM concordance model having infinite volume can also be read off from Figure 11. Since the distance to the surface of last scattering (SLS) is $L_{\text{SLS}} = \Delta \eta L_H \simeq 14.2\text{Gpc}$ where $\Delta \eta = \eta_0 - \eta_{\text{SLS}} = 3.329$ ($\eta$ is the conformal time), topologies above $L \simeq 6.6$ are so large that the SLS fits completely inside the toroidal universe. For larger models the value of $I(L)$ saturates at the infinite limit $L \to \infty$.

Figure 11. The weighted temperature correlation difference $I(L)$ is computed from the four correlation functions $C(\vartheta)$ shown in Figure 7. The length $L$ denotes the size of the cubic topology measured in units of the Hubble length.
corresponding to the concordance model. For all four values of $N_{\text{inter}}$ the correlation function $C(\vartheta)$ is in much better agreement with a cubic universe with $L$ slightly below 4 than with the infinite LCDM concordance model. The application of the modified Liu-Li mask has little influence on the ratio of $I(L)/I(\Lambda \text{CDM})$ for the minimum near $L = 4$ which is due to the fact that $C(\vartheta)$ is practically unchanged over the large interval from $\vartheta \simeq 50^\circ$ up to $\vartheta \simeq 165^\circ$ and below $\vartheta \simeq 30^\circ$. Excluding more pixels, i.e., decreasing $N_{\text{inter}}$ form 200 to 60, produces a more pronounced second minimum around $L \simeq 2$ which lies for $N_{\text{inter}} = 60$ below the value of the concordance model but above the absolute minimum near $L = 4$. This new feature is caused by the diminished power of $C(\vartheta)$ for angles $\vartheta$ in the interval $[30^\circ, 50^\circ]$ leading to a $C(\vartheta)$ with a power suppression already above $\vartheta \simeq 30^\circ$ instead of the usual $60^\circ$.

5. Summary

The presently best full-sky maps of the cosmic microwave background radiation are obtained by WMAP whose receivers are differential radiometers measuring the difference between two telescope beams separated by about $141^\circ$. Liu and Li [7, 8] discuss the possibility that the inclusion of hot pixels in the map-making process causes a bias in those pixels corresponding to a scan ring of about $141^\circ$. Due to the large diameter of the scan rings, the affected pixels lie in a region far from the galactic plane which is usually considered to be scarcely contaminated. Here we confirm the bias found in [7, 8] and, furthermore, compute the temperature two-point correlation function $C(\vartheta)$ by taking this bias into account. The most dramatic effect of these biased pixels is the so-called correlation hole at $\vartheta = 180^\circ$ in $C(\vartheta)$, which is absent by eliminating sufficiently many affected pixels. Thus, a correlation function $C(\vartheta)$ is obtained which displays almost no correlations above all angular scales larger than $60^\circ$.

In Figures 4–11, we have presented our results for the modified Liu-Li mask using the threshold temperature $T_{\text{thres}} = 1000 \mu K$ and employing the KQ75 mask. We have checked that the conclusions of this paper remain the same if the KQ85 mask is used instead of the KQ75 mask and, furthermore, if the calculations are performed for the thresholds $2000 \mu K$ and $4000 \mu K$, respectively.

Using the correlation function $C(\vartheta)$ based on the most reliable data, a test for a universe with a cubic topology is carried out. It is found that such a model fits $C(\vartheta)$ better than the LCDM concordance model if the side length $L$ of the cubic fundamental cell is slightly smaller than $L = 4$ measured in units of the Hubble length. For alternative models which can lead to a suppression of large scale power see e.g. [23, 24].

Acknowledgments

HEALPix (healpix.jpl.nasa.gov) [25] and the WMAP data from the LAMBDA website (lambda.gsfc.nasa.gov) were used in this work. The computations are carried out on the Baden-Württemberg grid (bwGRiD).
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