Measurement of the $t\bar{t}$ Production Cross Section in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV in the All Hadronic Decay Mode

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We report a measurement of the $t\bar{t}$ production cross section using the CDF II detector at the Fermilab Tevatron. The analysis is performed using $311 \text{ pb}^{-1}$ of $p\bar{p}$ collisions at $\sqrt{s} = 1.96 \text{ TeV}$. The data consist of events selected with six or more hadronic jets with additional kinematic requirements. At least one of these jets must be identified as a $b$-quark jet by the reconstruction of a secondary vertex. The cross section is measured to be $\sigma_{t\bar{t}} = 7.5 \pm 2.1^{\text{ (stat.)}} \pm 2.3^{\text{ (syst.)}} \pm 0.4^{\text{ (lumi.)}} \text{ pb}$, which is consistent with the standard model prediction.

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I. INTRODUCTION

At the Tevatron, the dominant standard model mechanism for top quark production in $p\bar{p}$ collisions is predicted to be $q\bar{q}$ annihilation to $t\bar{t}$. The top quark decays immediately into a $W$ boson and a $b$ quark almost 100% of the time. The $W$ boson subsequently decays to either a pair of quarks or a lepton-neutrino pair. The measurement of the $t\bar{t}$ cross section tests the QCD calculations for the pair production of a mas-
sive color triplet. These calculations have been performed in perturbation theory at the next-to-leading order \cite{1}. Recent work on corrections for soft gluon emission show that their effect on the cross section is small, and that they reduce the theoretical uncertainty due to the choice of renormalization and factorization scale. The total theoretical uncertainty is approximately 15%. At $\sqrt{s} = 1.96$ TeV, the predicted $t\bar{t}$ production cross section is 6.1 pb for a top mass of 178 GeV/c$^2$, the average value of the Run I measurements \cite{2}.

In this analysis, we examine events with an all-hadronic final state characterized by a six-jet topology. In the standard model top decay, this final state has the advantage of a large branching ratio of 4/9 and of being fully reconstructed. The major drawback is that it competes against a very large QCD multijet background which dominates the signal by three orders of magnitude after the application of the online trigger selection. To improve the signal-to-background ratio, a set of requirements based on the kinematic and topological characteristics of standard model $t\bar{t}$ events is applied to the data. In order to extract the $t\bar{t}$ signal, we select those jets identified as originating from $b$ quarks using a secondary vertex $b$-tagging algorithm, thus reaching a signal-to-background ratio of about 1/5. The CDF and DØ collaborations previously measured the $t\bar{t}$ production cross section in the all-hadronic channel \cite{3} using datasets with integrated luminosities of approximately 110 pb$^{-1}$ collected at $\sqrt{s} = 1.8$ TeV during Run I of the Fermilab Tevatron Collider. The results reported here are based on the data taken with the CDF II detector between March 2002 and September 2004, corresponding to an integrated luminosity of 311 pb$^{-1}$.

This measurement complements other recent $t\bar{t}$ cross section determinations by CDF in Run II using dilepton \cite{4}, lepton-plus-jets events \cite{5,6,7,8}, and lepton events \cite{4}. The organization of the paper is as follows. Section II contains a brief description of the CDF II detector. The trigger and the sample selections are described in Section III along with the acceptance associated with the optimized kinematic selection. The $b$-tagging algorithm and its efficiency for tagging $b$ jets are described in Section IV. In Section V the method for estimating the background from multijet processes is applied to the data and the related systematic uncertainties are evaluated. The $t\bar{t}$ production cross section measured in events with at least one $b$-tagged jet after the kinematic selection is presented in Section VI and the final result is summarized in Section VII.

II. THE CDF II DETECTOR

The CDF II detector \cite{9} is an azimuthally and forward-backward symmetric apparatus designed to study $p\bar{p}$ collisions at the Fermilab Tevatron. It uses a cylindrical coordinate system as described in \cite{10}. It consists of a magnetic spectrometer surrounded by calorimeters and muon detectors. The charged particle tracking system is immersed in a 1.4 T magnetic field parallel to the $p$ and $\bar{p}$ beams. A set of silicon microstrip detectors provide charged particle tracking in the radial range from 1.5 to 28 cm. A 3.1 m long open-cell drift chamber, the central outer tracker (COT), covers the radial range from 40 to 137 cm. The COT provides up to 96 measurements of the track position with alternating axial and $\pm 2^\circ$-stereo superlayers of 12-wire layers each. The fiducial region of the silicon detector extends to pseudorapidity $|\eta| \leq 1$, while the COT provides coverage for $|\eta| \leq 1$.

Segmented electromagnetic and hadronic calorimeters surround the tracking system and measure the energy of interacting particles. The electromagnetic and hadronic calorimeters are lead-scintillator and iron-scintillator sampling devices, respectively, covering the range $|\eta| \leq 3.6$. They are segmented in the central region ($|\eta| < 1.1$) in towers of $15^\circ$ in azimuth and 0.1 in $\eta$, and the forward region ($1.1 < |\eta| < 3.6$) in towers of 7.5$^\circ$ for $|\eta| < 2.11$ and 15$^\circ$ for $|\eta| > 2.11$.

The electromagnetic calorimeters \cite{11,12} are instrumented with proportional and scintillating strip detectors that measure the transverse profile of electromagnetic showers at a depth corresponding to the expected shower maximum. The measured energy resolution for electrons in the electromagnetic calorimeters are $14\%/\sqrt{E_T} + 1\%$ in the central and $16\%/\sqrt{E_T} + 1\%$ in the forward \cite{13} where the units of $E_T$ are GeV. We also measure the single-particle (pion) energy resolution in the hadronic calorimeters to be $75\%/\sqrt{E_T}$ for the central and $80\%/\sqrt{E_T} + 5\%$ for the forward detector \cite{14}. Jets are identified as a group of electromagnetic and hadronic calorimeter clusters which fall within a cone of radius $\Delta R = \sqrt{\Delta\phi^2 + \Delta\eta^2} \leq 0.4$ \cite{15}. Drift chambers located outside the central hadronic calorimeters and behind a 60 cm iron shield detect muons with $|\eta| \leq 0.6$ \cite{16}. Additional drift chambers and scintillation counters detect muons in the region $0.6 < |\eta| < 1.5$. Gas Cherenkov counters with a coverage of $3.7 < |\eta| < 4.7$ measure the average number of inelastic $p\bar{p}$ collisions and thereby determine the luminosity \cite{17}.

III. MULTIJET EVENT SELECTION

The all-hadronic final state of $t\bar{t}$ events is characterized by the presence of at least six-hadronic jets from the decay of the two top quarks. A multijet trigger relying on calorimetric information was specially developed to collect the events used in this analysis. After a preliminary selection of well contained and well reconstructed multijet events, tight kinematic requirements are imposed to reach a reasonable signal-to-background ratio.
A. Multijet Trigger Levels

CDF uses a three-level trigger system, the first two consisting of special purpose electronics and the third level consisting of conventional computer processors. For triggering purposes the calorimeter granularity is simplified to a $24 \times 24$ grid in $\eta, \phi$ space and each trigger tower spans approximately $15^\circ$ in $\phi$ and $0.2$ in $\eta$ covering one or two physical towers. At level 1, a single trigger tower is required with $E_T \geq 10$ GeV, while at level 2 we require that the total transverse energy, summed over all the trigger towers, $\sum E_T$ be $\geq 125$ GeV and the presence of four or more clusters each with transverse energy $E_T \geq 15$ GeV. Finally, the third trigger level confirms the level 2 selection using more accurate determination of the jet energy, requiring four or more reconstructed jets with $E_T \geq 10$ GeV. This trigger rate corresponds to an effective cross section of about $14$ nb and a efficiency of about $63\%$ for all $t\bar{t}$ events, and of about $85\%$ in the case of all-hadronic $t\bar{t}$ decays. The signal-to-background ratio $(S/B)$ for $t\bar{t}$ events after this selection is about $1/3500$ (assuming $\sigma_{t\bar{t}} = 6.1$ pb).

B. Preselection Requirements

After full-event reconstruction, we retain only those events that are well contained in the detector. We require the primary event vertex to be well reconstructed and to lie inside the luminous region ($|z| < 60$ cm). Jets are identified using a fixed-cone algorithm with a cone radius of 0.4 in $\eta - \phi$ space. The jet energies are corrected for detector response variations in $\eta$, detector stability, and energy loss in the uninstrumented regions. After a small correction for the extra energy deposited by multiple collisions in the same accelerator bunch crossing, a correction for calorimeter non-linearity is applied so that the jet energies correspond to the most probable in-cone hadronic energy. Each of these steps has an individual systematic uncertainty that is added in quadrature to derive the total uncertainty which decreases from 8 to 3% with increasing jet energy. After these corrections the jet energy provides a good estimate of the initial parton energy. This can be verified comparing the jet energy to the energy of an electromagnetic object such as a prompt photon or a $Z$ boson produced in the same event. For this analysis, jets are required to have $E_T \geq 15$ GeV and $|\eta| \leq 2$ after all corrections have been applied. We define the signal region by selecting events with a number of jets $6 \leq N_{jets} \leq 8$ in order to optimize the signal fraction. In order to minimize the contamination of this sample from the $t\bar{t}$ leptonic channels, we veto events containing any well identified high-$p_T$ electrons and muons as defined in $[8]$ and require that $\frac{E_T}{\sqrt{\sum E_T}}$ be $< 3 \sqrt{\text{GeV}}$ $[19]$, where the $E_T$ is corrected for both the momentum of any identified muons and the position of the $p\bar{p}$ collision point and the $\sum E_T$ is obtained by summing the $E_T$’s of all the selected jets. After these requirements 364,006 events are selected for further analysis.

C. Kinematic Selection Optimization and Acceptance

We define a kinematic selection based on dynamical and topological properties of the event. Quantities used are the number of jets, $N_{jets}$, the total transverse energy of the jets, $\sum E_T$, and the quantity $\sum_3 E_T \equiv \sum E_T - E_T^{-1} - E_T^{-2}$, obtained by removing the contribution of the two jets with the highest $E_T$ from the total $\sum E_T$. Other discriminant variables considered are the centrality $C$, defined as $C = \frac{\sum E_T}{\sqrt{s}}$, where $\sqrt{s}$ is related to the energy of the hard scattering process as inferred from the all-jets invariant mass; and the aplanarity $A$, defined as $A = \frac{1}{2} Q_1 Q_2$, $Q_1$ being the smallest of the three normalized eigenvalues of the sphericity tensor $M_{ab} = \sum_j p_{ja} p_{jb}$ calculated in the centre-of-mass system of all jets, where $p_j$ is the jet momentum. In order to model the signal we use PYTHIA v6.2 $[21]$ and HERWIG v6.4 $[22]$ leading-order Monte Carlo generators with parton showering followed by a simulation of the CDF II detector. The reference top mass chosen for the optimization is $m_{top} = 178$ GeV/$c^2$. The background behavior is obtained from the multijet data events: this is possible since the signal fraction at the initial stage is very small, $\sim 4\%$ at most. Comparisons of the background-dominated data and Monte Carlo generated signal events for the chosen kinematic variables are shown in Fig. $[11]$.

The kinematic selection is optimized for the maximum signal significance for $t\bar{t}$ events, defined as the ratio between the expected signal and the statistical uncertainty on the sum of signal and background. The values for the cuts after optimization are: $A \geq 0.005 \sum_3 E_T \geq 0.96$, $C \geq 0.78$, and $\sum_3 E_T \geq 280$ GeV. Such a selection yields 3315 candidate events in the data with an efficiency of 67% $\pm$ 1.4% for the $t\bar{t}$ signal and with a signal-to-background ratio $S/B \sim 1/25$.

The effect of the selection on the inclusive sample of $t\bar{t}$ events is summarized in Table $[11]$. The relative contribution from the leptonic channels after all the cuts is small, about 4%. The distribution of the data events as a function of jet multiplicity is shown in Table $[11]$.

Note that the requirement of the multijet trigger coupled with those of the kinematic selection modify the monotonicaly falling multiplicity spectrum of QCD background production processes.

The systematic uncertainties affecting the $t\bar{t}$ acceptance are summarized in Table $[11]$. The systematic uncertainty of 19.4% arising from the jet energy scale
is dominant, since this analysis requires the presence of a large number of jets in the event which are used to build the set of kinematic variables employed in the selection. We also study the effects on the efficiency of different Monte Carlo physics generation schemes, initial and final state radiation ISR/FSR, and the variation of parton distribution functions PDFs within their uncertainties.

IV. \(b\)-TAGGING IN THE MULTIJET SAMPLE

In order to further improve the signal-to-background ratio, we exploit the heavy flavor content of \(t\bar{t}\) events using a \(b\)-tagging algorithm based on secondary vertex reconstruction as described in detail in \cite{5, 23}. The algorithm identifies jets containing a \(b\)-hadron state by reconstructing its decay vertex with at least two good quality tracks with hits in the silicon vertex detector. A \(b\)-tagged jet must have an associated secondary vertex with a significance larger than 7.5, where the typical resolution of the vertex displacement is about 190 \(\mu\)m. The efficiency to tag real \(b\) quarks and the average number of tags per event, \(n_{\text{tag}}\), the quantities used in the cross section calculation, are measured in \(t\bar{t}\) Monte Carlo events after the complete kinematic selection. The method we use takes into account the different tagging efficiencies for jets coming from the fragmentation of \(b\)-, \(c\)-, or light-flavored quarks. The rates for all possible combinations of heavy- and light-flavored jets in the events are measured and used to properly combine the different efficiencies. This is particularly
important in the case of all-hadronic $t\bar{t}$ decays since we find that about 44% of the events after the kinematic selection contain a charm quark from a $W$ boson in a top decay and 17% of the events contain two charmed quarks. In Table IV we summarize the heavy flavor fractions in $t\bar{t}$ Monte Carlo events after kinematic selection. The efficiency calculation includes the correction factors 0.91 ± 0.06 for $b$ jets and 0.91 ± 0.12 for $c$ jets respectively. These factors account for the different efficiency measured in data and Monte Carlo events; their measurement is described in detail in [5].

We find that the average number of tags present in a $t\bar{t}$ event after kinematic selection is $n_{\text{avg}} = 0.846 ± 0.073$. The systematic uncertainty is dominated by the uncertainty of the data to Monte Carlo correction factors for tagging $b$ and $c$ jets, where the uncertainties on both factors are considered fully correlated.

| Number of $c$ jets | 0   | 1   | 2   |
|--------------------|-----|-----|-----|
| Number of $b$ jets |     |     |     |
| 0                  | 0.11 ± 0.01 | 0.18 ± 0.02 | 0.08 ± 0.01 |
| 1                  | 3.62 ± 0.07 | 5.95 ± 0.09 | 2.37 ± 0.06 |
| 2                  | 27.53 ± 0.17 | 43.37 ± 0.19 | 16.80 ± 0.14 |

V. BACKGROUND ESTIMATE

The background sources for this final state are due mainly to QCD production of heavy-quark pairs ($b\bar{b}$ and $c\bar{c}$) and false tags from light-quark jets. Other standard model processes such as $W/Z$+jets can be neglected due to the smaller production cross section and small acceptance due to the selection cuts.

Given the theoretical uncertainties related to the production cross section for the generation of $N$-parton events, it is important to have a method for the background estimate that does not require any Monte Carlo information, and thus, is based solely on data. The method we use is based on the fact that even if the relative contribution from different processes changes as a function of jet multiplicity, the probability that a fiducial jet, a jet with two good quality tracks in the silicon detector, is tagged is approximately constant with increasing multiplicity. This assumption allows us to use the tag rate extracted from events depleted in $t\bar{t}$ signal as a measure of the tag rate in events with higher jet multiplicity. The depleted events are taken to be those with exactly four jets.

The tag rate per jet is evaluated in this $N_{\text{jets}} = 4$ sample and is parameterized in terms of variables sensitive to both the efficiency for true heavy-flavored objects and the rate of false tags. These variables are jet-$E_T$, the number of tracks reconstructed in the vertex detector associated to the jet, $N_{\text{trk}}$, and the number of primary vertices in the event, $N_{\text{vert}}$. The tag rates per jet as a function of these variables are shown in Fig. 2.

![Fig. 2: Tag rate for fiducial jets as a function of jet $E_T$, jet $N_{\text{trk}}$, and $N_{\text{vert}}$.](image)
acteristics with respect to those found in the sample with exactly four jets, where the parametrization has been derived. This selection modifies the jet-$E_T$ and $\eta$ spectra so that the average tag rate per event for jets from QCD background becomes higher. However, the parametrization of the tag probability in terms of properties of the jet ($E_T$, and $N_{\text{trk}}$) is shown to describe well this increase for the kinematic selection. Possible biases due to the selection are treated as systematic uncertainties on the background prediction with the help of different control samples depleted in signal contribution. A specific control sample is defined for extracting the systematic uncertainty on the background determination due to each kinematic variable. The control sample is obtained by applying the (N - 1) kinematic selection cuts, and reversing the selection requirement on the chosen variable under study. For instance, in the case of the systematic error due to the $\sum E_T$ requirement, we apply the standard cuts on all other variables, and additionally require $\sum E_T \leq 280$ GeV. With this method we measure a relative systematic uncertainty of 4.1% on the background estimate due to the kinematic selection by summing in quadrature the uncertainties obtained separately for each kinematic variable. The contributions from running conditions, such as instantaneous luminosity and detector configuration, have been studied and found to be negligible. After the application of the kinematic selection to a multijet sample of 311 pb$^{-1}$ we are left with 3315 events with $6 \leq N_{\text{jets}} \leq 8$ in which there are 816 tags in 695 events. The distribution of observed tags and events for the different jet multiplicities is shown in Table IV.

After kinematic selection, the expected background is 717 ± 29 tags. However, since this background estimate is obtained from all the events passing the selection before tagging we need to subtract the contribution due to the $t\bar{t}$ events. This amount is derived with an iterative procedure using the $t\bar{t}$ cross section from the data, that is the observed excess divided by the average number of tags. After this correction, the number of tags expected from background sources is reduced to 683.7 ± 37.5 tags.

![FIG. 3: Average number of tags per event observed in the multijet sample before kinematic selection compared with the estimate from the tag rate parametrization.](image)

![FIG. 4: Number of tags observed in multijet data after kinematic selection compared with the expected background. The $t\bar{t}$ expectation refers to the measured cross section of 7.5 pb.](image)

### VI. CROSS SECTION MEASUREMENT

The excess of the observed data over the background in the signal region shown in Table VII is ascribed to $t\bar{t}$ production. A measurement of the cross section can be extracted from the acceptance and the background estimate:

$$\sigma_{t\bar{t}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{\epsilon_{\text{kin}} \times n_{\text{tag}}^{\text{ave}} \times \mathcal{L}_{\text{int}}},$$

where $N_{\text{obs}} = 816$ and $N_{\text{bkg}} = 684\pm38$ are the number of total observed and background tags, respectively, in the signal region $6 \leq N_{\text{jets}} \leq 8$, $\epsilon_{\text{kin}} = 6.7 \pm 1.4\%$ is the signal kinematic selection efficiency shown in Table IV, $n_{\text{tag}}^{\text{ave}} = 0.846 \pm 0.073$ is the average number of tags in $t\bar{t}$ events and $\mathcal{L}_{\text{int}} = 311 \pm 18$ pb$^{-1}$ is the integrated luminosity. The value of the $t\bar{t}$ cross section is: $\sigma_{t\bar{t}} = 7.5\pm2.1(\text{stat.})^{+3.3}_{-2.2}(\text{syst.})^{+0.5}_{-0.4}(\text{lumi.})$ pb for a top mass of 178 GeV/$c^2$. In Fig. 4, the distribution of the number of observed tags and background is compared to the $t\bar{t}$ signal expectation assuming the production cross section measured in this analysis.

The cross section is also measured for different top quark mass assumptions as shown in Table VII. In the same table are reported the kinematic efficiency...
TABLE V: Observed number of tags and expected background and signal after the kinematic selection. Only one cumulative value is given for the corrected background in 6 \leq N_{\text{jet}} \leq 8 because the iterative correction is applied to all the entries in the signal region.

| Jet Multiplicity | 4          | 5              | 6              | 7              | 8
|------------------|------------|----------------|----------------|----------------|
| Background       | 18.27 \pm 0.55 & 139.6 \pm 5.8  | 283.5 \pm 11.7  | 284.9 \pm 11.7  | 148.8 \pm 6.1  |
| Corrected Background | 17.6 \pm 0.3  & 133.4 \pm 7.8  | 683.7 \pm 37.5  |                |                |
| \( t\bar{t} \) (\( \sigma = 6.1 \text{ pb} \)) | 0.5 \pm 0.1   | 14.7 \pm 3.2    | 52.9 \pm 11.6   | 39.3 \pm 8.6    | 13.8 \pm 3.0    |
| Data             | 20         | 154            | 346            | 322            | 148            |

and the relative systematic uncertainty due to the jet energy scale. The dependence of the average number of tags on \( m_{\text{top}} \) has been found to be negligible.

TABLE VI: Kinematic selection efficiency, relative systematic uncertainty from jet energy scale (JES), and measured cross section for different top quark mass assumptions.

| \( m_{\text{top}} \) (GeV/c^2) | \( \epsilon_{\text{kin}} \) (%) | JES Syst. (%) | \( \sigma \) (pb) |
|-------------------------------|----------------------------------|--------------|-----------------|
| 165                           | 5.1 \pm 1.1                      | 22.1         | 9.9^{+4}_{-1}   |
| 170                           | 5.8 \pm 1.1                      | 21.2         | 8.7^{+4}_{-3}   |
| 175                           | 6.3 \pm 1.3                      | 20.1         | 8.0^{+4}_{-3}   |
| 180                           | 6.9 \pm 1.3                      | 18.8         | 7.3^{+4}_{-3}   |
| 185                           | 7.6 \pm 1.3                      | 17.1         | 6.6^{+3}_{-2}   |

VII. CONCLUSIONS

Using an optimized kinematic selection and a b-jet-identification technique, we are able to improve the S/B of the initial multijet sample obtained with a dedicated trigger from 1/3500 to 1/5. With the selected sample, we measure the production cross section for \( t\bar{t} \) events in the all-hadronic final state to be \( \sigma_{\text{\( t\bar{t} \)}} = 7.5 \pm 2.1 \text{(stat.)}^{+3.3}_{-2.2} \text{(syst.)}^{+0.5}_{-0.4} \text{(lumi.)} \text{ pb} \) assuming \( m_{\text{top}} = 178 \text{ GeV/c}^2 \). These results agree well with the standard model expectation of \( \sigma_{\text{\( t\bar{t} \)}} = 6.1 \text{ pb} \) for the same value of the top mass and with the results obtained in the leptonic channels. The current all-hadronic measurement is dominated by systematic uncertainties. The increase in integrated luminosity we expect from Run II will not only reduce the statistical uncertainty but will also allow for a more stringent selection with a better signal-to-background ratio. In particular the application of strategies based on neural network selection and the requirement of two identified b-quark jets per event can help to achieve a signal-to-background ratio of about 1/1 and a significant reduction in the systematic uncertainty.

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