Field sources near the southern-sky calibrator PKS B1934-638: effect on spectral line observations with SKA-MID and its precursors

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ABSTRACT
Accurate instrumental bandpass corrections are essential for the reliable interpretation of spectral lines from targeted and survey-mode observations with radio interferometers. Bandpass correction is typically performed by comparing measurements of a strong calibrator source to an assumed model, typically an isolated point source. The wide field-of-view and high sensitivity of modern interferometers means that additional sources are often detected in observations of calibrators. This can introduce errors into bandpass corrections and subsequently the target data if not properly accounted for. Focusing on the standard calibrator PKS B1934-638, we perform simulations to assess this effect by constructing a wide-field sky model. The cases of ASKAP (0.7–1.9 GHz), MeerKAT (UHF: 0.58–1.05 GHz; L-band: 0.87–1.67 GHz) and Band 2 (0.95–1.76 GHz) of SKA-MID are examined. The use of a central point source model during bandpass calibration is found to impart amplitude errors into spectra measured by the precursor instruments at the ∼0.2–0.5 per cent level dropping to ∼0.01 per cent in the case of SKA-MID. This manifests itself as ripples in the source spectrum, the behaviour of which is coupled to the distribution of the array baselines, the solution interval, the primary beam size, the hour-angle of the calibration scan, as well as the weights used when imaging the target. Calibration pipelines should routinely employ complete field models for standard calibrators to remove this potentially destructive contaminant from the data, a recommendation we validate by comparing our simulation results to a MeerKAT scan of PKS B1934-638, calibrated with and without our expanded sky model.

Key words: techniques: interferometric.

1 INTRODUCTION
The radio source PKS B1934-638 (J2000 19h39m25.02671s–63d42m45.6255s) is a compact steep spectrum source (see e.g. O’Dea 1998) associated with Seyfert 2 type galaxy at a redshift of z = 0.183 (Holt, Tadhunter & Morganti 2008). It is heavily relied upon as a primary calibrator source for radio interferometers in the Southern hemisphere as it is extremely stable (Ojha et al. 2004), exhibits no structure on scales larger than ∼40 milliarcsec (Tzioumis et al. 2010), and is effectively unpolarized (Hugo, private communication), with limits:

\[
\frac{Q^2 + U^2}{I^2} \approx -32 \text{ dB}
\]

and

\[
\frac{Q^2 + U^2 + V^2}{I^2} \approx -30 \text{ dB}.
\]

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Bandpass calibration in the context of radio interferometry is the process of correcting the frequency-dependent instrumental response. The gain of the instrument as a function of frequency is imparted primarily due to the response of electronic components in the signal path. Every independent receiver chain will have a different response, thus each element in the array (and each feed in an individual element) will require a unique bandpass correction, with the general assumption being that the instrumental bandpass is stable in time relative to the duration of a typical observation. Bandpass corrections are generally derived by making a scan of a calibrator source whose spectral and temporal behaviour is well known. A set of antenna-based corrections are derived from the baseline-based visibility measurements by averaging the scan in time and solving for the complex gain in each channel against a model of the calibrator source. In the case of PKS B1934-638 the model is a point-source with a spectrum as shown in Fig. 1 (Reynolds 1994).

Calibration of the bandpass shape is essential to reliably recover the intrinsic structure of astrophysical spectral lines, with experiments demanding high dynamic range requiring a bandpass correction that also achieves an appropriately high signal-to-noise ratio. Errors in these multiplicative antenna-based bandpass corrections propagate into the baseline spectra of target sources when the calibration is applied. For modern broad-band radio interferometers even 'continuum' observations require accurate bandpass correction as the broad bandwidths are relied upon for the sensitivity boost that they provide when the whole band is imaged using multifrequency synthesis techniques (e.g. Sault & Conway 1999).

In the sections that follow we test the suitability of using simple model of PKS B1934-638 for the dish-based mid-frequency component of Phase I of the Square Kilometre Array (SKA-MID), as well as its precursor instruments the Australian Square Kilometre Array Pathfinder (ASKAP; DeBoer et al. 2009) and MeerKat (Jonas & MeerKat Team 2016). These instruments have high instantaneous sensitivity and large fields of view due to a combination of technological advances in receiver technology, and the use of dishes in the 12–15 m diameter range. Thus the assumption that a simple point-source calibrator is well-matched to the measurements may not be valid for all observational scenarios due to the contributions to the measurements from other sources in the field. Previous studies have been made on the effects on incomplete sky models during continuum self-calibration (e.g. Grobler et al. 2014), however here we consider the effect whereby errors are transferred to a target in the spectral domain via calibration tables due to incomplete modelling of a calibrator source. The frequency ranges over which we perform the tests are also marked in Fig. 1. These are 0.7–1.9 GHz (ASKAP; DeBoer et al. 2009), 0.58–1.05 GHz (MeerKat UHF and L-band respectively; Jonas & MeerKat Team 2016), and 0.95–1.76 GHz (SKA-MID Band 2; Dewdney et al. 2013).

We construct a model of the field sources surrounding PKS B1934-638 using high dynamic range images from ASKAP and the Australia Telescope Compact Array (ATCA). We then use a simulation to test the effect that using an incomplete (central point-source only) model has on the derived bandpass corrections, and how these errors propagate into the target spectral line observations.

2 SKY MODEL CONSTRUCTION

We used two observations in order to construct a model of the field around PKS B1934-638. The first of these is an image formed using all of the calibrator scans of PKS B1934-638 taken prior to the Compact Array Broad-band Backend (Wilson et al. 2011) upgrade to the ATCA in order to form a deep, narrow-band image of the field at 1.4 GHz. Only arrays in the 6 km configurations were chosen in order to maximize the angular resolution for morphological characterization of sources close to the primary target. The second data set is a deep (~12 h) integration of the field using the Boolardy Engineering Test Array (BETA; Hotan et al. 2014) with a frequency range of 711–1015 MHz, for a central frequency of 863 MHz. The image formed from this observation allows the detection of sources out to a radius of approximately 2 deg from the primary target.

We made no attempt to modify the standard models used for PKS B1934-638 itself. Self-calibration of the data followed standard procedures, with the BETA data being split into four separate sub-bands. The Reynolds (1994) model of PKS B1934-638 was used as a starting point for both the BETA and the ATCA data. Self-calibration was performed in several iterations using initial, conservative phase-only solution intervals to prevent the suppression of field sources. Following each iteration, the sky model was expanded to include new components as they emerged in the improved images, until no further improvement to the dynamic range of the images was discernible. Calibration of the ATCA and BETA data was performed using the DIFMAP (Shepherd 1997) and MEQTREEs (Noordam & Smirnov 2010) packages, respectively. The final images from which the model catalogue was constructed are shown in Fig. 2.

A sky model consisting of point and Gaussian components was derived in a hierarchical fashion. Features in the images were decomposed into such components using the PyBDSF source finder (Mohan & Rafferty 2015), with the exception of the principal component, PKS B1934-638 itself, for which we simply adopted a point source with the polynomial fit to the spectrum derived by Reynolds (1994). To this we added the seven sources in the ATCA.
image found to exhibit complex morphologies, as labelled A–G in Fig. 2. PyBDSF used between 3 and 16 point or Gaussian components to characterize the extended structures. The BETA observations were used to estimate the total integrated flux densities of each source at 863 MHz and spectral indices were assigned accordingly. The third tier of sources are the point-like features.

3 EFFECT OF FIELD SOURCES ON BASELINE VISIBILITIES

3.1 An analytic example

Consider a point source calibrator at the phase centre with a flux density $S_0$, and a second source of flux density $S_1$ within the antenna primary beam at coordinate $(s_1,0)$. The analytic expression for the Fourier transform of these two unresolved sources gives us the visibility function

$$V(u(t,v),v(t,v)) = S_0 + S_1 e^{-i\phi},$$

where

$$\phi = 2\pi u(t,v)x_1.$$  

By Euler’s formula, the measured intensity is

$$|V(u(t,v),v(t,v))|^2 = S_0^2 + S_1^2 + 2S_0S_1\cos(-\phi)$$

and the phase term is:

$$\arg(V(u(t,v),v(t,v))) = \tan^{-1}\left(\frac{S_1\sin(-\phi)}{S_0 + S_1\cos(-\phi)}\right).$$

The intensity and phase in this simple example are periodic functions with a time and frequency dependence that is coupled to projected baseline length as well as the distance of the secondary source from the phase centre. For $S_0 \gg S_1$ the phase term will tend to zero, whereas for $S_0 \rightarrow S_1$ the phase term dependence becomes hour-angle dominated. Every off-axis source within the antenna or station primary beam contributes ‘ripples’ to the visibility function in this manner.

3.2 Simulation setup

Having derived the model in Section 2 we can demonstrate the effect of multiple additional field sources by simulating a realistic set of visibilities, and this process is the cornerstone of the tests that follow. An arbitrary set of visibilities was simulated by generating CASA (McMullin et al. 2007) format Measurement Set, containing time and frequency information, and a set of $(u,v,w)$ tracks appropriate for the array being simulated. For the antenna layouts for ASKAP please refer to Gupta et al. (2008), and for those of MeerKAT and SKA-MID Heystek et al. (2015). Once the Measurement Set was generated the data column was filled with a set of simulated visibilities based on the sky model. Since the sky model derived in Section 2 represents intrinsic brightness measurements the effects of the primary beam must be applied when predicting. This was implemented by applying a simple $(\cos^2)$ voltage beam appropriate for the dish sizes in the array (resulting in a $\cos^6$ pattern on the sky), which also captures the frequency dependence across the band. Our method includes proper treatment of the differing dish sizes of SKA-MID baselines that involve MeerKAT (13.5 m) and SKA (15 m) dishes. Note that the primary beam effects were not simulated using an image-plane treatment, but by application of a direction- and frequency-dependent Jones matrix during the visibility prediction stage. Since we are only examining the effects of the confusing sources we did not include thermal noise in any simulations. All

Figure 2. The upper left-hand panel shows the BETA image of the PKS B1934-638 field out to the nominal 10 per cent radius of the primary beam at 863 MHz. The greyscale is linear and runs from $-6$ to 30 mJy beam$^{-1}$. The dashed circle shows the extent of the ATCA image, cut at the 10 per cent primary beam level, and shown in the lower left-hand panel. Again the greyscale is linear, running from $-6$ to 30 mJy beam$^{-1}$. The seven sources that are not well characterized by single point or Gaussian components are marked A–G, with contour images for each presented in the right-hand column. The contour levels are $0.1 \times (3^0, 3^{0.5}, 3^{1.0}, 3^{1.5}, \ldots)$ mJy beam$^{-1}$. There are more contours associated with the region around source A as the primary beam correction has raised the image noise towards the edge of the map. Each of the seven sub-images spans $3 \times 3$ arcmin.

$V(u(t,v),v(t,v)) = S_0 + S_1 e^{-i\phi},$
3.3 Effect on visibility measurements

Fig. 3 shows the amplitudes of three baselines as a function of time (vertical axis) and frequency (horizontal axis) from an 8-h MeerKAT track using the full sky model. The simulation covers the full effective frequency range of the $L$-band receiver (900–1670 MHz). Left to right, the length of the baseline shown increases by a factor of approximately ten between each panel, with the de-projected baseline length indicated together with the relevant antenna pair. The underlying response to PKS B1934-638 is best seen on the right-hand panel. As expected for a point source at the phase centre, the primary calibrator source is stable in time with a minimum signal-to-noise ratio of 3 being required to avoid a solution being flagged. The reference antenna is set to the first one present before a solution is attempted for a given antenna, and all of the data will be averaged in time, and the measured visibilities will be compared to a predicted set of model visibilities in order to derive antenna-based corrections for each frequency channel.

A typical scan made for bandpass calibration purposes will (depending on the science requirements) last for several minutes. All of the data will be averaged in time, and the measured visibilities will be compared to a predicted set of model visibilities in order to derive antenna-based corrections for each frequency channel. We have briefly demonstrated above the level to which field sources around PKS B1934-638 will affect the visibility function in the case of MeerKAT, with the true response of the instrument (not including thermal noise) during a calibration scan being akin to an appropriate subset of the long track shown, and quite clearly differing from the response to an isolated point source.

4 PERTURBATIONS TO THE INSTRUMENTAL BANDPASS CORRECTIONS

The plots in this section show the perturbations to the instrumental bandpass corrections that result from assuming a model that consists only of PKS B1934-638. For each of the scenarios under test a set of ’observed’ visibilities is generated using the process described in Section 3, featuring the sky model derived in Section 2. Bandpass corrections are then generated using the CASA BANDPASS¹ task, which returns a set of per-channel antenna-based gain corrections that minimize the difference between the ’observed’ visibilities and the point model. Task defaults were used, with the principal relevant parameters being the minimum of four baselines being present before a solution is attempted for a given antenna, and a minimum signal-to-noise ratio of 3 being required to avoid a solution being flagged. The reference antenna is set to the first one in the Measurement Set, which for all of the instruments considered will be on that is close to the centre of the array. The bandpass solutions were not normalized.

We generated these simulated corrections for the frequency ranges of the instruments under consideration, namely ASKAP, MeerKAT ($L$-band and UHF), and SKA-MID (Band 2), and the results are shown in Fig. 4, with the relevant array labelled on each panel. Each of the four scenarios are presented, with a pair of panels separately showing the amplitude and phase of the complex antenna-based bandpass corrections as a function of frequency, for each instrument that we simulate. The colours represent the average deprojected length of the baselines formed with each antenna, running from blue (shortest) to red (longest).

For Fig. 4 the simulation is conducted with a bandpass integration time of 5 min, with hour angle coverage that has the target field transiting at the mid-point, i.e. the point at which PKS B1934-638

¹ Version 5.1.1
Figure 4. Complex (amplitude and phase) bandpass corrections for (top to bottom) ASKAP, MeerKAT L-band, MeerKAT UHF, and SKA-MID Band 2 as a function of frequency, derived from 5 min calibrator scans centred at transit. These plots represent the errors introduced into the bandpass by calibrating with a sky model that consists only of PKS B1934-638. The summed lengths of the (de-projected) baselines that an antenna contributes to have been determined, and are coloured from shortest (blue) to longest (red). Note the differing scales on the y-axes for these panels. Please refer to Section 4 for details. A colour version of this figure is available online.
can be observed with the longest projections of baseline length on the sky (given the location of the array on the earth).

Since the true instrumental bandpass in this simulation is a unity response with an amplitude of one and a phase of zero, and given that we do not include the effects of thermal noise, the plots represent the errors imparted to the instrumental bandpass corrections purely due to the effects of using an incomplete sky model for the field.

The main notable features in Fig. 4 are intuitively connected to the visibility effects described in Section 3:

(i) Errors in the antenna-based bandpass corrections become more severe for antennas that have shorter total baseline lengths. This is due to the higher fringe rates on longer baselines washing out the contribution from confusing sources over the averaging interval used to derive the bandpass corrections.

(ii) The effect becomes more severe with decreasing frequency, where the field sources have an increasing contribution due to the expansion of the primary beam, and the spectral turnover of the primary calibrator source. This is most readily seen by comparing the MeerKAT UHF and L-band plots, where there is both a higher absolute amplitude and phase error, as well as increased spread in the longer baselines for the former.

(iii) Large-scale modulations across the band are likely due to the large number of short spacings in these core-heavy arrays dominating the solutions. SKA-MID has much longer baselines and in greater numbers than either ASKAP or MeerKAT. These serve to mitigate this large-scale modulation in the case of SKA-MID. The large number of long baselines will see less contribution from field sources due to fringe rate effects. These two factors serve to reduce both the absolute errors in the bandpass, and flatten the large-scale response in frequency, however the antennas involved in shorter baselines still exhibit the large-scale variations.

Using the ASKAP example, we qualitatively demonstrate the effect of using longer averaging intervals, and different hour angle coverage in Figs 5 and 6. The longer averaging intervals will affect the bandpass errors due to time-smearing effects reducing the influence of far-field sources, particularly on the long baselines. The hour-angle variations will change the projection of the array on the sky, thereby affecting the effective baseline distribution.

For Fig. 5 we repeated the full-band ASKAP simulation presented in Fig. 4, but increased the observation length to 10 (upper amplitude and phase plots) and 15 min (the lower pair). Marginal improvement is seen in the absolute errors, and the large-scale modulation in frequency also persists. Since the short baselines dominate the solutions (at least in the case of both ASKAP and MeerKAT) this is to be expected. Furthermore, since longer averaging intervals affect not only the visibility amplitudes on the longer baselines but also preferentially wash out sources further from the field centre, the minimal improvement in absolute error from a longer averaging time can be further explained by considering the sky model derived in Section 2. Referring to Fig. 2, after PKS B1934-638 the most dominant sources are by far the pair of bright FR-II (Fanaroff & Riley 1974) sources, labelled C and D, which are in relatively close proximity (as projected on the sky) to the primary calibrator source. Indeed it is these two sources that contributed mainly to the modulation of the baseline dynamic spectra presented in Fig. 3.

We repeated the 5 min ASKAP simulation from Fig. 4, however this time simulated an observation that occurs when the target field is at an elevation of 20 deg. The resulting complex bandpass
corrections as a function of frequency are shown in Fig. 6, for direct comparison to the corresponding transiting simulation shown in the upper two panels of Fig. 4. Again the improvement in the absolute error is marginal, however the large-scale structure in frequency has changed. This we explain in terms of the different projection of the array on to the sky providing a very different effective baseline distribution compared to the transiting case.

5 EFFECT OF INCOMPLETE MODEL ON SPECTRAL LINE OBSERVATIONS

Having shown the level at which an incomplete model introduces errors into the bandpass correction, we now demonstrate how these errors propagate into the target visibilities when the bandpass is applied, and thus the errors introduced into the spectrum of a target source. To show this we generated model visibilities consistent with a 1 Jy flat spectrum point source at the phase-centre (zero phase response for all baselines), and applied the appropriate corrupted bandpass table using the CASA APPLYCAL task. We then took the perturbed (‘corrected’) visibilities and examined their vector-averaged spectrum. The results are shown for ASKAP, MeerKAT UHF, and MeerKAT L-band in Fig. 7, and for SKA-MID Band 2 in Fig. 8, expressed as percentage error in the true source spectrum.

5.1 Effects of hour-angle coverage and duration of calibrator scan

The effects of hour-angle (elevation) and averaging interval during the bandpass observation are captured in Fig. 7. The blue and red traces represent transit and 20 deg elevation scenarios respectively, and for the transit scenario the different shades of blue represent integration times of 5, 10, and 15 min (light to dark). The integration time effect for the 20 deg case is omitted for clarity.

As expected, the behaviour of these plots mimics those of the bandpass tables, with the visibility per baseline corrupted by the multiplicative bandpass amplitude errors from the two elements involved on a per-channel basis. Broad features (widths of $\sim 20$ MHz) are artificially introduced into the spectra, corrupting the large-scale behaviour of the spectral baseline response at the $\sim 0.1$ per cent level for ASKAP and MeerKAT, dropping to the $\sim 0.01$ per cent level for SKA-MID. Comparing the red curves to the blue curves shows that
the morphology of this large-scale corruption is coupled to the array layout (or projected array layout as modified by elevation effects). Increasing the length of the calibrator scan primarily affects the higher frequency structure in the spectral errors, mainly due to the longer averaging interval suppressing the contribution of off-axis sources to the longer baselines.

The large-scale error in the source spectrum due to incomplete modelling of the bandpass calibrator field is a direction-independent effect that will apply equally to all sources in an image cube, and would be difficult to remove using further continuum subtraction techniques as in all cases it would not be well-described by a low-order polynomial.

The higher frequency structure in the introduced errors is perhaps more insidious. Although the fractional error is smaller for this component, the widths are narrower and could mimic genuine spectral line emission or absorption features in high dynamic range observations. This is particularly true for the SKA-MID case, as shown in Fig. 8. The lower panel shows a 100 MHz region of the full spectrum shown in the upper panel. The dark lines show the mean line widths for H I discs at the corresponding redshift, as predicted by Obreschkow et al. (2009). Interpretation of spectra of the radio continuum emission, and thus in addition to apparent spectral line corruptions, continuum subtraction under the assumption of a smooth model also becomes inappropriate. As an example, the continuum emission of a typical star forming galaxy with a H I-to-continuum flux density ratio of 2:1 will exhibit corruptions at a comparable level to the examples above.

5.2 Effects of imaging weights

The core-dominated antenna layouts for the three arrays considered in our simulations mean that for most imaging applications a significant downweighting of the core spacings must be applied in order to condition the point spread function (PSF) for reliable deconvolution. This is generally achieved by tuning of the robustness parameter (\( r \)) Briggs (1995). The vector-averaged visibility spectra derived above are equivalent to imaging with purely natural weighting of the visibilities, so here we investigate how the incomplete sky model affects target spectra for a range of different weighting schemes.

The robustness parameter facilitates a continuous transition between natural weighting (\( r = 2.0 \)), for which every visibility has unity weighting, and uniform weighting (\( r = -2.0 \)) for which every grid cell in the \((u,v)\) plane has unity weighting. Thus for \( r < 2.0 \) the inevitably higher density of samples close to the origin of the \((u,v)\) plane means that shorter spacings are preferentially downweighted. The principal motivation is to trade-off sensitivity against angular resolution or PSF sidelobe levels. Since we have established that use of an incomplete calibrator model imparts errors that are directly coupled to the intrinsic (or projected) baseline distributions of the arrays, we can expect the robustness parameter to directly modify the behaviour of the spectral perturbations.

The process for testing this is as above, i.e. a corrupted bandpass table is generated and applied to a simulated set of target visibilities. At the final stage, instead of extracting the corrupted spectrum directly from the visibilities, an image cube is produced using CASA’s CLEAN task, and the spectrum is measured from the cube. The sky in our simulations consists only of a point source at the phase centre, thus wide-field imaging corrections are not required. However in order to capture the effects of visibility weighting in a realistic manner,\(^2\) we use an image size of \(8192 \times 8192\) pixels, each of which is \(1.5\) arcsec \(\times 1.5\) arcsec. Wide-band deconvolution schemes are also not required, as we are treating each channel independently in order to obtain a full spectral measurement, and indeed given the properties of the simulated sky, the spectrum is measured directly from the brightest pixel in the dirty (i.e. not deconvolved) cube.

The imaging process is repeated for \( r \) values of \(-1.5\), \(-1.0\), \(-0.5\), 0.0, 0.5, 1.0, and 1.5. Since this is a somewhat computationally expensive simulation we test only the case of MeerKAT 1-band, and then only for 2000 frequency channels between 1020 and 1060 MHz. Again, the extracted spectrum is recast in terms of the percentage error from the true source spectrum, and the results for the seven different weighting schemes are shown in Fig. 9.

\(^2\)For most imaging software the resolution (and PSF sidelobe levels) for any weighting scheme other than natural will depend on the image size (in pixels) and the angular extent of each pixel, as these parameters subsequently set the size and resolution of the grids in the \((u,v)\) domain. Weighting schemes other than natural use cell-based rather than visibility-based weights, and so adjusting the \((u,v)\) grid properties changes how the visibilities are distributed amongst the cells.
Figure 9. A subset of the MeerKAT L-band simulation showing the percentage error in the spectrum of a target source as a function of frequency, for seven different values of the robust parameter. The robust parameters are colour coded as per the legend. A colour version of this figure is available online.

As $r$ values tend towards uniform weighting the high-frequency ripples in the perturbations become more pronounced, as expected for the effect being coupled to the longest baselines in the array. This also suggests that the magnitude of the high frequency ripples highlighted for SKA-MID in Section 5.1 represent the best case scenario, as for just about all practical imaging applications the core-spacings will have to be suppressed, significantly so for SKA-MID science cases that require subarcsecond angular resolution.

The overall characteristics of the low-frequency component of the introduced spectral errors do not significantly change with varying $r$ parameters. The maximum–minimum error in the examples shown here changed by a few tens of per cent, however this is probably irrelevant given the more significant effect that changing the hour-angle / elevation of the calibrator scan has on this particular aspect of the spectral perturbations.

6 A REAL-WORLD TEST CASE

Our simulation framework and the results derived in this paper are validated using a calibration scan of PKS B1934-638 from the MeerKAT telescope. The observation used 55 antennas, with an on-source time of 8 min, observed at an elevation angle of approximately 38 deg. The correlator was configured to deliver 4096 frequency channels. Flagging was done using the CASA FLAGDATA task. Autocorrelations and visibilities with amplitudes of exactly zero were discarded. The low-gain edges of the band (850–900 and 1658–1800 MHz) were flagged. The initial integration (8 s) was discarded to mitigate against incomplete slewing and antenna settling time, and visibility amplitudes greater than 100 were flagged. Regions with strong persistent radio frequency interference (RFI; 944–947, 1160–1310, and 1476–1611 MHz, primarily due to geolocation satellites) were flagged for baselines shorter than 1000 m. The RFLAG and TFCROP algorithms within FLAGDATA were then used to automatically identify and remove residual RFI from the remaining visibilities using the default settings. Following this a bandpass correction was derived and applied using a model containing only PKS B1934-638. The two auto-flagging algorithms were then re-run on the residual (corrected – model) visibilities, and the initial bandpass corrections were discarded. The bandpass corrections were then repeated by calibrating against a model that consisted only of PKS B1934-638 and then a set of model visibilities generated in accordance with the simulation method (Section 3.2). The differences between the two resulting bandpass tables are shown in Fig. 10. The level and structure of the residual bandpass differences are in excellent agreement with those predicted by the simulation, and shown in the MeerKAT L-band case in Fig. 4. Some discontinuities are present which are likely due to residual RFI.

7 CONCLUSIONS

The general assumption when calibrating radio interferometer data is that calibrator sources are isolated point sources at the phase centre. However the instantaneous sensitivity and wide fields of view of modern radio telescopes may make this assumption inappropriate for many observational scenarios. We have investigated how unmodelled field sources surrounding the typical southern-sky primary calibrator PKS B1934-638 introduce errors into the bandpass corrections, and subsequently the spectra of science targets for observations with ASKAP, MeerKAT, and SKA-MID.

The bandpass tables derived from an incomplete model of the PKS B1934-638 field when transferred to the visibilities of the science target impart spectral corruptions with a range of scales. These corruptions are multiplicative at the antenna level, and thus affect the spectra of all sources in the field (including broad-band continuum emission) at a level that is commensurate with their brightness.

The behaviour of the errors is coupled to the array layout, with the shorter baselines of the array governing the behaviour of the lower frequency corruptions, and the longer baselines giving rise to higher frequency components. The projection of the baselines on to the sky also means that the error patterns have a strong elevation dependence. Increasing the integration time of the calibrator scan (within reasonable limits) preferentially reduces the higher frequency components, as the higher fringe rates of longer baselines effectively suppress off-axis sources via smearing effects. The use of weighting schemes that tend towards uniform however amplifies...
these high frequency errors, as more weight is given to the longer baselines in this regime.

With reference to Figs 7 and 8 the broad, low frequency component of the spectral corruptions would need to be mitigated to achieve spectral baseline accuracies of greater than approximately 1 part in 1000 for the precursor instruments, and 1 part in 10 000 for SKA-MID. Continuum subtraction using the typical method of a low-order polynomial fit along the frequency axis would likely be insufficient. The higher frequency component is particularly evident in the SKA-MID simulation. Although the high frequency perturbations exist on scales comparable to the line widths of H I discs at the cosmological redshifts the SKA and its precursors aim to probe, the amplitude of this component is small enough such that it is only likely to affect the brighter H I lines in the ultra-deep tiers of SKA-MID surveys.

To provide some brief realistic examples (with η being an efficiency term, and $T_{sys}$ being the assumed system temperature):

(i) A hypothetical local H I observation with MeerKAT: A 20 h on-source integration at 1.4 GHz, with 22 kHz channels and $T_{sys}/\eta = 22$ K has a naturally weighted channel noise of 0.11 mJy beam$^{-1}$. Thus the 0.1 per cent maximum bandpass error equals the image noise for a 110 mJy continuum source.

(ii) A hypothetical deep H I observation at $z \simeq 0.3$ with MeerKAT: A 200 h on-source observation at 1.1 GHz, with $T_{sys}/\eta = 23$ K and 100 kHz channels has a naturally weighted channel noise of 18 μJy beam$^{-1}$. In this example the 0.1 per cent maximum bandpass error equals the image noise for a 18 mJy continuum source, something that is relatively common given the field of view.

The straightforward way to mitigate all of the issues we have investigated here is of course to expand the models of this field, and indeed all standard calibrator fields. This recommendation is supported by the results of Section 6, which shows the difference between a bandpass table generated with a single point source model and one generated with our full-field model in the case of a real MeerKAT $L$-band calibration scan of PKS B1934-638. The residual structure is remarkably similar to the predicted corruptions for this scenario shown in Fig. 4.

Initial results from MeerKAT’s UHF system (Hugo, private communication) suggest that the contribution from very strong sources in the sidelobes of the primary beam is significant, and this is an effect that our simulations do not capture due to the simple primary beam model. The use of full-field models that include strong sources in the sidelobes of the antenna primary beam patterns will thus be particularly important for MeerKAT UHF and SKA-MID Band 1, the latter of which we have not considered here. An apparent sky model constructed via an observing campaign for each precursor instrument and the SKA itself would contain any uncertainties in the primary beam model from the problem, in so far as the primary beams of alt/az mounted dishes exhibit azimuthal symmetry. Even simply including sources C and D (Fig. 2) will greatly reduce the issue at $L$-band / SKA Band 2 frequencies, as these two sources dominate the visibility perturbations for all scenarios considered here.

Another approach we have not investigated here is the use of (u, v) range selection to remove the more error-prone shorter baselines from the calibration procedure. This has been shown to be effective during self-calibration of arrays with high concentrations of antennas in the core, where the shorter baselines may pick up large-scale emission features that are difficult to model via deconvolution-based techniques.

Finally, we note that we have only examined this effect in the context of the PKS B1934-638 field. A cursory examination of other fields has shown that the errors resulting from an incomplete model of this field are comparatively small. For example, typical MeerKAT calibration observations of PKS 0407-65 and 3C 286 close to transit will introduce errors of up to 1 percent (a factor of a few tens larger) due to incomplete modeling. The conclusion drawn in the previous paragraph naturally applies to all primary calibrator fields.
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