The H I opacity of the intergalactic medium at redshifts $1.6 < z < 3.2$

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1 INTRODUCTION

The mean optical depth of the H I Lyα forest observed in the spectra of high-redshift quasi-stellar objects (QSOs) is one of the main pieces of information on the physical state of the intergalactic medium (IGM). This is because the optical depth of the Lyα forest ($\tau_{\alpha}$) is sensitive to the combination of a wide variety of effects that we can collect under two main headings (Rauch et al. 1997). First, $\tau_{\alpha}$ is sensitive to all the familiar parameters of the cosmological model, including $\Omega_\Lambda$, $\Omega_m$, $\Omega_b$, the Hubble parameter and the parameters that describe the primordial power spectrum of density fluctuations. These parameters determine the density of hydrogen per unit length, the conversion from Mpc to wavelength in a spectrum and the spatial variations of the density. The second set of parameters are astrophysical, rather than primordial, and they determine the ionization and thermal state of the low-density hydrogen. The IGM is highly photoionized by ultraviolet photons from early stars and active galactic nuclei. $\tau_{\alpha}$ is then sensitive to the evolution of the intensity and spectrum of the ultraviolet (UV) background or UVB. The energy input per photoionization, and the competition between photoheating and the cooling from the adiabatic expansion together give the temperature of the low-density IGM, an output rather than an input parameter.

Over the last decade numerical hydrodynamic simulations of the IGM have steadily improved in accuracy. We can now make artificial QSO spectra directly from the full hydrodynamical simulations and measure the statistical properties of the Lyα forest absorption in those spectra. As expected, we find that the absorption in the artificial spectra depends on the complete set of cosmological and astrophysical parameters. In Tytler et al. (2004b, hereafter T04b) and Jena et al. (2005, hereafter J05) we showed how we can choose sets of input parameters for simulations that give artificial spectra that are statistically equivalent to the largest and best samples of real spectra. We can now use the simulations to decode the IGM.

When we match simulations to real QSO spectra we obtain joint constraints on the full set of cosmological and astrophysical parameters that we input to the simulations. We do not obtain constraints on individual input parameters, except when we fix all the many other parameters at values obtained from other observations.

We find that the statistical properties of the Lyα forest are highly sensitive to many of the input parameters (Tytler et al. 2004b; Bolton et al. 2005; Jena et al. 2005). When we compare to calibrated real spectra, we can expect to obtain joint constraints on sets of parameters that are competitive with the best measurements from other types of observations. This motivates us to improve the accuracy of the measurement of the IGM.

We also find that the comparison between numerical simulations and real spectra of the Lyα forest provides the most accurate
measurements of the intensity of the UVB (Rauch et al. 1997; Tytler et al. 2004b; Bolton et al. 2005; Jena et al. 2005).

We have found that two statistics in particular provide a good summary of the Lyα forest. One is the effective optical depth τ_eff and the other some measure of the clumping and temperature of the gas, such as the linewidth distribution or the power spectrum of the QSO flux. In T04 we measured τ_eff to high precision over the redshift range 1.6 < z < 2.2. The aim of this paper is to extend the redshift range over which we can make detailed comparisons between simulations and data by providing a calibrated and precise measurement of the H I Lyα forest opacity over the redshift range 2.2 < z < 3.2.

1.1 Previous work

There has been extensive previous work dedicated to measuring the total amount of absorption in the Lyα forest, summarized in part by T04b and Meiksin & White (2004) and the references therein. Many of these measurements appear to differ, but Meiksin & White (2004) showed that much, but not all, of the disagreement between some measurements was caused by differences in treating errors. T04b discuss other differences that remain.

Although we have had spectra of the Lyα forest since 1972, it is only recently that we have had simulations of the quality to match highly accurate measurements of the mean amount of absorption.

The mean absorption is hard to measure for three reasons discussed at length in T04b: the continuum level, metal lines and sample size.

To measure the amount of absorption we must first guess the continuum prior to the absorption. This is relatively easy at z ≲ 2, hard at z ≃ 3 and very hard at z > 4, where there is little if any unabsorbed continuum remaining in the Lyα forest. T04b dealt with the continuum level by making and fitting artificial spectra that looked similar to the real spectra. They saw and fitted the emission lines in the Lyα forest of each individual spectrum (Tytler et al. 2004a). These lines vary a lot from one QSO to another (Tytler et al. 2004a; Suzuki et al. 2005). Using the artificial spectra we were able to show that their continuum level was accurate to approximately 0.3 per cent, after correction, and averaging over the Lyα forest of 77 QSOs.

The simulations that we compare to the Lyα forest spectra typically lack the resolution and physics required to give realistic metal absorption lines and Lyα lines from regions with column densities log N_{HI} > 17.2 cm^{-2}. We then need a prescription for dealing with metal lines and strong Lyα lines in the Lyα forest. Some measurements ignore these lines, while others subtract some or most of them. At z = 1.9 T04b showed that the metal lines contributed 15 per cent and strong Lyα lines 7 per cent of the absorption in the Lyα forest. However, they each contributed approximately the same amount to the total variance of the absorption as did the Lyα absorption in the low-density IGM.

The last requirement for an accurate measurement of the mean amount of absorption in the Lyα forest is a large sample, ideally at least tens of QSOs. It had long been noted that there is conspicuous variation in the amount of Lyα forest absorption from QSO to QSO (Carswell et al. 1982; Kim, Cristiani & D’Odorico 2001), and T04b showed that the amount of variation on scales of Δz = 0.1 (121 Å in the observed frame) is consistent with large-scale structure for a primordial spectrum of perturbations with slope n = 0.95, and present amplitude σ_8 = 0.9.

Following Oke & Korycansky (1982), we define DA(z) = 1 − F(z), where F (z) is the observed flux divided by the continuum level, and F(z) is the mean over many spectra at a given redshift. T04b found that DA (z = 1.9) = 0.151 ± 0.006, including all absorption at rest-frame wavelengths 1070–1170 Å towards 77 QSOs. The error here is partly from the continuum level, and partly from the sample size. T04b estimated the metal line absorption from wavelengths between the Lyα and C IV emission lines, from both their own spectra and from the spectra of Sargent, Boksenberg & Steinbel (1988). They estimated the strong Lyα lines from the statistics of such lines in other spectra. When they subtracted both the metal lines and strong Lyα lines, the DA drops to 0.118 ± 0.010. T04b estimated that approximately five ideal spectra, all at the same z_{em} with no continuum errors, and no metal lines or strong Lyα lines, would give DA with an error of 0.01 at a single redshift, z = 1.9. High-resolution spectra might approach this limit.

In Jena et al. (2005) we presented a set of 40 fully hydrodynamic simulations of the IGM at z = 2. We derived scaling laws that related the parameters of simulated spectra to the parameters that we input to the simulations. When we apply the scaling laws to a simulation, we can predict the output parameters to higher accuracy than the typical measurement error in real spectra. We were able to predict the most common linewidth (b-value) to 0.3 km s^{-1} and τ_eff to 0.0027, both approximately a factor of 4 smaller than the measurement errors in the real spectra. In this paper we address the need for improved measurements.

1.2 Our approach

We apply the methods of T04b to make a calibrated measurement of DA at 2.2 < z < 3.2. The basic idea is that we will ensure that our continuum fitting is unbiased by simultaneously fitting our real data and artificial spectra that have been carefully prepared to exhibit the types of errors shown in real spectra. The hope is that any systematic errors in our continuum fitting will manifest themselves in our continuum fits to both the real data and the artificial data. We can then measure them in the artificial data and apply the appropriate corrections to our real data.

We will generally follow the details of T04b, with some specific exceptions. Here we made artificial continuum and emission-line spectra using principal-component spectra, rather than real Hubble Space Telescope (HST) spectra (Suzuki et al. 2005). We made the Lyα forest absorption from randomly placed Voigt profiles with parameter distribution functions taken from the literature, instead of using a simplified model of the IGM to produce the Lyα forest absorption. In addition, we added metal and strong Lyα lines to the artificial spectra. However, the main difference is that we now use the high-resolution echelle spectrometer on the Keck 10-m telescope (HIRES) spectra with 8 km s^{-1} resolution in place of the 250 km s^{-1} resolution spectra that we used in T04b. The higher resolution comes with many times more photons per Å and allows us to place accurate continua at higher redshifts.

2 DATA SAMPLE

We use a collection of QSO spectra obtained with the HIRES spectrograph on the Keck telescope (Vogt et al. 1994). These spectra were collected between 1994 and 2004, for a variety of programmes. The 24 QSOs that we use in this paper were selected from among our HIRES spectra for the following reasons: (1) they have significant

1 DA is the Lyα forest absorption.
Table 1. HIRES Lyα forest spectra used to measure DA.

| Identifier | RA (B1950) | Dec. (B1950) | z_em | V |
|------------|------------|--------------|------|---|
| q001+8118  | 00 14 04.45| +81 18 28.6| 3.366 | 16.50 |
| q004+2627  | 00 42 06.42| −26 27 45.3| 3.289 | 18.47 |
| q100+1300  | 01 00 33.38| +13 00 12.1| 2.681 | 16.57 |
| q105+1619  | 01 05 26.97| +16 19 50.1| 2.640 | 16.90 |
| q109+1432  | 01 19 16.21| +14 32 43.2| 2.870 | 16.70 |
| q130+4021  | 01 30 50.28| −40 21 51.0| 3.023 | 17.02 |
| q139+0008  | 01 39 40.85| +00 08 17.8| 3.405 | 18.32 |
| q301+0035  | 03 01 07.70| −00 35 03.0| 3.231 | 17.62 |
| q302+3213  | 03 22 11.8| −32 13 34.6| 3.302 | 17.95 |
| q364+1310  | 03 46 54.0| −13 10 9.0| 2.300 | 16.50 |
| q364+1645  | 04 49 59.00| −16 45 09.0| 2.677 | 17.00 |
| q074+2414  | 07 41 42.05| +47 41 53.4| 3.210 | 17.50 |
| q093+2858  | 09 30 41.40| +28 58 53.0| 3.428 | 17.50 |
| q100+3638  | 10 05 44.13| +36 38 02.4| 3.125 | 17.85 |
| q115+2640  | 11 55 07.62| +26 40 37.0| 2.850 | 17.60 |
| q120+1539  | 12 00 57.62| +15 39 36.1| 2.981 | 17.10 |
| q120+1601  | 12 08 23.81| +10 11 08.5| 3.822 | 17.90 |
| q124+3047  | 12 43 44.90| +30 47 54.0| 2.560 | 17.00 |
| q124+3143  | 12 44 48.83| +31 43 02.9| 2.961 | 17.90 |
| q132+3927  | 13 20 41.02| +39 27 46.8| 2.985 | 17.06 |
| q133+2123  | 13 37 47.92| +21 23 54.1| 2.700 | 17.90 |
| q222+2024  | 22 23 13.32| +20 24 58.5| 3.560 | 18.38 |
| q233+1845  | 23 37 13.08| +18 45 12.2| 2.620 | 17.00 |
| q234+1229  | 23 44 13.2| +12 28 50.0| 2.784 | 17.50 |

Figure 1. The number of HIRES QSOs which have complete Lyα forest coverage in different redshift bins.

3 ARTIFICIAL SPECTRA

We attempted to make artificial spectra that mimic real spectra in every important way, including emission lines, cosmic ray hits, echelle blaze and flux calibration errors. For each real spectrum, we made four artificial spectra with the same redshift and noise properties and various absorption lines.

We made the unabsorbed continuum shape, including emission lines with the principal-component spectra described by Suzuki et al. (2005). The artificial spectra have a wide variety of shapes, and include realistic emission lines between Lyα and Lyβ. The exact shape and strength of the emission lines was different for each artificial spectrum.

We made the HI absorption from discrete lines, with the line distribution functions given in Kirkman & Tytler (1997). The artificial spectra used in this paper have lines of all column densities, \(10^{19} < N_{HI} < 10^{19.5}\) cm\(^{-2}\), and we placed lines at random redshifts, from the \(z_{em}\) listed in Table 1, down to zero redshift.

If a real spectrum had a damped Lyα (DLA) with \(\log N_{HI} > 10^{19.5}\) cm\(^{-2}\), we added a line with the same \(\log N_{HI}\) at the same wavelength to all the accompanying artificial spectra.

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With each HI absorber, we also added the strong doublet absorption lines of C IV, Si IV and Mg II to the artificial spectrum. We held the H i/X column density ratio constant for each metal ion, and the width of each metal absorber was calculated by assuming that the H i b values were entirely thermal. This resulted in an artificial metal forest that was superimposed on the HI forest, which made the artificial spectra look more realistic when inspected closely.

The artificial spectra used in this paper were generated differently from the spectra we used for the same purpose in T04b. The spectra in T04b were generated via a toy model of the IGM that mimicked the large-scale structure, but we did not add the metal lines of the Lyα lines of Lyman-limit systems.

We added noise to the artificial spectrum and attempted to match the approximate S/N level of each real spectrum. We based the noise levels in our simulated spectra upon the estimated error estimates in the real echelle spectra. The resulting artificial spectra have a S/N ratio similar to their real spectra except for three of the five with S/N > 45, where the artificial ones have a S/N ratio that is too low by approximately 1.5.

We also added a blaze effect to the artificial noise levels to simulate the increased S/N ratio obtained at the centre of each echelle order. Furthermore, we added small fluxing errors, by offsetting different echelle orders by the blaze function multiplied by a Gaussian random deviation with \(\sigma = 2\) per cent, which is larger than the expected fluxing errors in the data (Suzuki et al. 2003). In Fig. 2 we show an example of artificial spectra, below the real spectra they approximate.

Although we see differences between our artificial and real spectra, they do not concern us. Since we placed the Lyα lines at random redshifts, the artificial spectra lack large-scale structure. The artificial spectra also show more total absorption than real spectra, generally \(\sim 5\) per cent more total absorption over the redshift range 2.4 < \(z\) < 3.0. As we show in the next section, we are able to fit continua very well for a wide range of total absorption, so we do not believe that the minor differences between our real spectra and the artificial ones have significantly changed our results.

4 CONTINUUM FITTING

Four undergraduate authors, SH, KJ, CM and GS, took a training program to fit QSO continua. They fitted artificial QSO spectra...
that were not matched to any specific QSO. These spectra had a variety of emission redshifts, S/N ratio, emission-line profiles and flux calibration errors. The four all fit the same spectra, and after they completed a few spectra, we revealed the true continuum level and we discussed their fit. Within a few weeks two of them were able to fit continua as well as any of us.

After this training had been completed, we asked them to fit the real and matched artificial spectra. We provided spectra in sets comprising one real spectrum and two artificial ones matched to that real one. Each fitter was given the same copy of the real spectrum, but different versions of the artificial spectra. We did not reveal which was the real spectrum in a set.

The results indicate that the two best fitters were excellent. The other two fitters were less accurate, and more importantly, occasionally had large fitting errors. Thus for the measurement of DA, we used the average continuum of the two best fitters, and do not discuss the results of the other two fitters any further.

The standard deviation of the continuum fit errors per spectral segments of length $\Delta z = 0.1$ is 1.2 per cent. We fit a total of 96 artificial spectra, four per QSO (two per fitter per QSO), and there were a total of 275 segments of length $\Delta z = 0.1$ in these artificial spectra. Averaged over all 275 segments, the continua of the two best fitters were above the true continua by 0.29 per cent. If the fits were unbiased, and the errors per segment were uncorrelated we would expect the bias to be $0.29/\sqrt{275} = 0.07$ per cent. As in T04b we have measured a small bias.

In Fig. 3 we show a weak correlation between the error in the continuum fit to the artificial spectra and their S/N ratio. We have not measured whether the bias varies from object to object, or as a function of $z$.

Based upon our ability to continuum fit artificial spectra, we conclude that errors in continuum placement are not a significant source of error when measuring DA in high-resolution, moderate S/N ratio spectra at $z < 3.0$.

5 MEASUREMENT OF THE MEAN FLUX

To avoid confusion between multiple Lyman series lines, we restrict our analysis to the region between the Ly$\alpha$ and Ly$\beta$ emission lines of each QSO. To avoid continuum fitting problems associated with rapidly changing emission-line profiles, and possible contamination from the proximity effect, we further restrict our measurement of DA to the rest-frame wavelengths 1070–1170 Å.

5.1 Removal of LLS absorption

Because many of our objects were originally observed as part of our programme to measure the primordial deuterium abundance, which can only be measured in Lyman Limit System (LLS: including DLAs), our data contains more LLS absorption than would a completely random sample. This prevents us from removing the LLS absorption statistically, as we did in T04b. To overcome this problem, we have masked out all regions of each spectrum containing Ly$\alpha$ absorption associated with identified LLS. By mask, we mean that the pixels were marked as being unusable, and were not used in any further computations. In practice, our LLS identifications are probably not complete, but we believe that we identified and masked all absorbers with $N_{\text{HI}} > 10^{19}$ cm$^{-2}$.

If the QSO was originally observed as part of our primordial D/H programme, we also masked out any metal lines that might be at the known redshift of the targeted LLS. All wavelengths within 2000 km s$^{-1}$ of an H$\alpha$, CIV, SiIV, CIII, SiIII, CII or SiII transition at the D redshift were masked. The transitions were masked based solely on the redshift, the transition rest wavelength, and the fact that there is metal absorption associated with the system in which we had searched for D. No attempt was made to fit the metal absorption.
5.2 Removal of metal line absorption

We have not attempted to identify and mask individual metal lines in the Lyα forest. While many of the spectra used in this paper have enough S/N ratio to identify some of the absorption in the Lyα forest, manual removal of metal absorption is likely to be very incomplete, and we will not know how much absorption was missed. Instead, we will use the method described in T04b, and subtract the metal absorption statistically. In this section we use the notation from T04b, summarized in table 1 of that paper. Briefly, DM refers to the amount of absorption from metal line alone, and DM4 refers to the DM from metal lines listed in table 3 of SBS88 averaged into bins of size Δz = 0.1.

We have measured the amount of absorption from metal lines in spectra published for 52 QSOs in Sargent et al. (1988, hereafter SBS88). We previously did this in section 8.1 of T04b for 26 QSOs with 1.7 < z_em < 2.3. We now add the remaining QSOs listed in SBS88, to cover 1.7 < z_em < 3.54. We sum the equivalent widths of all the metal lines listed for the 52 QSOs in table 3 of SBS88 from rest wavelengths of 1225–1500 Å. We group the lines in bins of length 121.567 Å in the observed frame, corresponding to Δz = 0.1 for Lyα. In T04b we called these DM4 values. We now have 354 DM4 values, with a mean of 0.0191 ± 0.0017 and σ(DM4) = 0.0312, both slightly larger than the values (mean 0.0167 ± 0.0022, σ = 0.0274) in T04b. The mean observed wavelength is now 4764.4 Å, compared with 4124.8 Å in T04b.

We attempted to remove all absorption lines from systems that appeared to be associated with the QSOs. These systems produce large broad absorption line like lines that are concentrated in certain emission lines, including Si iv, N v and O vi. The Si iv and especially the N v lines can contribute a lot to the DM estimate. However, the lines of these associated systems will have little effect on the total metal absorption in the DA region because O vi is excluded. We found six QSOs with conspicuous strong associated N v absorption that was responsible for many of the largest DM measurements of any segments in the sample. We also removed all lines from systems with β = v/c < 0.01, corresponding to velocities within 3000 km s^{-1} of the QSO. This value is large enough to remove most associated systems, without removing too many intervening systems. This criterion removed Si iv from six additional QSOs, and a few C ii and Si ii lines. We also removed the occasional Galactic Ca ii at zero redshift. After removing these absorption lines, the mean DM decreased 18 per cent to 0.0157 ± 0.0013 and the standard deviation decreased 21 per cent to σ(DM4) = 0.0248.

Following T04b, we re-fitted the DM4 values as a function of wavelength in the rest frame of the QSO λ_o and observed wavelength λ_o:

\[ \text{DM5(λ_o)} = 0.01564 - 4.646 \times 10^{-5}(λ_o - 1360) \]  

and

\[ \text{DM6(λ_o)} = 0.01686 - 1.798 \times 10^{-6}(λ_o - 4158). \]  

[The slope of DM 6(λ_o) was erroneously listed as 7.136 × 10^{-5} per cent in T04b, equation (13), it should be 7.136 × 10^{-4} per cent]. These fits supersede those given in T04b, both because the sample is twice as large, and because we did not remove associated systems in T04b. Note that here we give the DM as absolute values, while in T04b we gave the DM values in percentages.

The removal of the associated systems has no significant effect on the intercepts, but a large effect on the slopes, because the N v lines concentrate near the minimum λ_o that we used from SBS88. Removing the associated systems without enlarging the sample causes a slight decrease in the slope with λ_o, while increasing the sample has no additional effect. For λ_o, half the decrease in the slope comes from the removal of the associated systems and the other half from the enlargement of the sample.

We want DM as a function of both λ_o and λ_i. We see a clear trend of DM increasing as λ_i decreases, but no significant trend with λ_o, and hence no strong evolution with z_em and z_abs. The tendency for DM to rise with falling λ_i is hard to see in plots, but appears to come from a smaller fraction of segments with no absorption lines at lower λ_i.

We choose to correct each bin, from Kast and HIRES, by the DM for its λ_o assuming it is at λ_o = 1120 Å. The DM values range from DM(1070) = 0.0291, to DM(1120) = 0.0268 in the centre of our λ_o range, to DM(1170) = 0.0245. In T04b we used DM 3 = 0.023 ± 0.005 for all segments. We now use DM (1120) = 0.0268, for all segments, and we simultaneously correct for the slight trend with λ_o given by equation (2). At the mean λ_o of the Kast sample we measure DM (3525) = 0.01799 while for the HIRES sample DM (4498) = 0.01624, both at the mean λ_o of the SBS88 sample: 1357.2 Å. We apply the λ_o correction by multiplying by τ eff (λ_o)/τ eff (4764.4 Å), where 4764.4 Å is the mean λ_o of the SBS88 sample. For example, we calculate τ eff at 4498 Å, to be 1.03 × 0.0276, corresponding to DM = 0.0276. As we explained in Jena et al. (2005), we subtract the τ eff values corresponding to the DM from the τ eff corresponding to the DA. We do not directly subtract DA—DM.

Since the DM values that we use are now larger than in T04b, the DA values are smaller, and the changes are most at the lowest z_abs.

Although we have improved upon T04b, we do not have a definitive measurement of DM. Three issues remain. First, we extrapolate in λ_o well beyond the limit of the data. Secondly, we use all the metal lines listed in SBS88, without regard for the equivalent width. Their S/N ratio was approximately constant with wavelength in the relevant wavelength range, other than an increase in the N v emission line. Since their spectra do not have the resolution or S/N ratio to see weak lines, the DM values we obtain from their spectra will be too small and our DA too large. Thirdly, our masking of the lines of LLS may leave too few metal lines compared with the DM from SBS88. This error would make our DA too small. We masked all the metals from one LLS in most QSOs. These QSOs were selected because they contained these LLS, and hence we expect that they would have excess metals if we did not apply this mask. However, some of a random sample of QSOs would have LLS by chance, and hence we may have overcorrected. This error will tend to cancel that from the numerous weak metal lines missed from the SBS88 line lists.

As a sanity check, we measured the amount of (unmasked) metal absorption in the six of our spectra that have significant coverage redward of the Lyα emission line. In those six spectra we measured the mean metal absorption over the observed wavelengths that correspond to the Lyα forest between 2.2 < z < 3.2 to be 2.1 per cent. This value probably has large errors associated with it because it has been measured from only six QSOs, but it does increase our confidence that our general metal line removal based on the results of SBS88 is not wildly inaccurate.

5.3 Measurement of mean DA in Δz = 0.1 spectral segments

After masking targeted deuterium systems and LLS with obvious Lyα lines, we measured the mean flux in spectral segments of Δz = 0.1. We started at a rest wavelength of 1070 Å (or the lowest wavelength with data in cases of incomplete spectral coverage) in each QSO, and computed the mean flux of all segments that are

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fully contained between the rest wavelengths of 1070 and 1170 Å. There are typically three \( \Delta z = 0.1 \) segments in an individual QSO spectrum. We discard incomplete segments and any segment with more than 10 per cent of its flux masked for any reason, e.g. a DLA in a spectrum will cause at least one, and frequently two segments in a given QSO spectrum to be discarded. Finally, we subtracted the anticipated metal absorption from each segment, as described in Section 5.2.

Our results are shown in Fig. 4, where we also show the results for the Kast spectra from T04b. Fig. 4 shows only the absorption of the low column density Ly\( \alpha \) forest – we have attempted to remove the Ly\( \alpha \) of all LLS and all metal line absorption for all the Kast and HIRES spectra. For both the HIRES and Kast spectra we subtracted the same mean amount of metal absorption from each Kast point. For the Ly\( \alpha \) of the LLS we subtracted the mean for all the Kast points, but we masked individual Ly\( \alpha \) lines for the HIRES points.

5.4 DA as a function of redshift

To tabulate the mean DA as a function of redshift, we binned the data shown in Fig. 4 into redshift bins of width \( \Delta z = 0.2 \). We estimated the mean DA of each bin to be simply the mean value of the points in the bin. We estimated the error to be the standard deviation of all the points (see Section 5.5), we compute the standard deviation from the best power-law fit to the data) divided by the square root of the number of points in each bin. Using the standard deviation of all points instead of the standard deviation of just the points in each bin gives nearly identical results for bins with large numbers of points, but seems to be much better behaved for bins with small numbers of points. Our results are in Table 2 and shown in Fig. 5.

DA as a function of \( z \) is well fitted by a power law of the form \( A (1 + z)^\gamma \). Minimizing \( \chi^2 \) to the points in Table 2 gives \( A = 0.0062 \) and \( \gamma = 2.75 \). The \( \chi^2 \) of the best fit is 8.69 and the reduced \( \chi^2 \) for seven degrees of freedom (nine data points, two parameters) is 1.24.

The dashed lines in Fig. 4 enclose the \( \pm 1 \sigma \) confidence interval fits. They are produced by taking the envelope that contains all power-law fits with \( \chi^2 < \chi^2_{\text{min}} + 2.3 \). Thus, the plotted error bounds are not power laws, but each point on the error curves corresponds to a point on a power law that fits our data. The last column in Table 2 gives the difference between the bounds divided by two.

We do not give errors for \( A \) or for \( \gamma \). The \( A - \gamma \chi^2 \) manifold is complex, and it is not well approximated by only two numbers (\( \sigma \) for \( A \) and \( \gamma \)). Attempts to do so in the past (Steidel & Sargent 1987; Press, Rybicki & Schneider 1993; Kim, Cristiani & D’Odorico 2001), have led to all sorts of confusion in the literature – consider the efforts of Seljak, McDonald & Makarov (2003) and Meiksin & White (2004) to determine the allowed values of \( \tau_{\text{eff}} \) at various redshifts. We recommend use of the results given in Table 2.

Note that the small dip in DA that we observed at \( z > 2.2 \) in fig. 22 of T04b is not present in the new HIRES data. The combined HIRES + KAST data seems to be well fitted by a single power law, and no significant deviations from a power law are present in our data.

5.5 Dispersion of DA in \( \Delta z = 0.1 \) spectral segments

The new points from this work show less dispersion than the points in T04b. This is consistent with the fact that we have removed LLS absorption before calculating the mean flux at each point, while T04b calculated the mean flux at each point with the LLS present, and then subtracted the LLS absorption statistically. While both results will give the same mean value for the H\( \text{i} \) Ly\( \alpha \) forest opacity,
the T04b method will include the substantial dispersion of the LLS absorption.

The standard deviation of the HIRES DA points (each covering $\Delta z = 0.1$) about the mean given by the power-law fit is $\sigma_{DA} = 5.2_{-0.8}^{+1.0}$ per cent over redshifts $2.2 < z < 3.2$. This $\sigma_{DA}$ value includes the intrinsic variance of the Ly$\alpha$ forest, the variance of metal line absorption (we removed the mean, not the individual metal absorption), and the variance of our continuum fitting errors. It should not include a significant contribution from LLS absorption, since we masked the Ly$\alpha$ absorption associated with LLS before measuring any DA values.

We can subtract variances (squares of standard deviations) to estimate the standard deviation of the absorption by Ly$\alpha$ from the low-density IGM alone. As in T04 Section 9, we work with mean values in segments of length $\Delta z = 0.1$. We now repeat the calculations given in T04, considering only the HIRES spectra. We take the standard deviation of the metal absorption as 3.7 per cent, where we have scaled the value of 3.1 per cent in table 4 of T04b by the mean metal absorption which is now DM = 2.76 per cent, up from 2.3 per cent. We also use the standard deviation of the continuum fitting errors, 1.2 per cent (Section 4). We find that the intrinsic variation of the mean amount of absorption in the Ly$\alpha$ forest over $\Delta z = 0.1$ segments is $\sigma (\Delta z = 0.1) / \sigma_{DA} = 3.4_{-0.5}^{+1.0}$ per cent. This value is a mean from the whole z range, centred near $z = 2.7$. At $z = 2.7$ the mean total DA per segment, including metals but not Ly$\alpha$ lines of LLS, is 0.246, and after subtracting the metals it drops to 0.2246.

The $\sigma (\Delta z = 0.1)$ value from HIRES spectra agrees with the value that we calculated in T04b (Section 9.3) for Kast spectra: $\sigma (\Delta z = 0.1) / \sigma_{DA} = 3.9_{-0.1}^{+0.3}$ per cent at $z = 1.9$. The error is larger now, because we have fewer DA measurements giving a larger error on the measurement of the standard deviation of the DA values. We expect that $\sigma (\Delta z = 0.1)$ will increase with increasing $z$ because the power spectrum of the flux in the Ly$\alpha$ forest increases with increasing redshift (Croft et al. 2002; McDonald et al. 2004). We do not see this, but this may be because our measurement errors are large and not well determined. In T04b we did not subtract the continuum fitting error because it appeared to be small, and was not well determined. We found contradictory evidence that the continuum fit error might be large, in which case the $\sigma (\Delta z = 0.1)$ value should be less than $3.9_{-0.1}^{+0.3}$ per cent.

We conclude that 24 QSOs are adequate to obtain the mean DA, but we would prefer far more QSOs to obtain an accurate measurement of the variance in the DA.

6 DISCUSSION

Our DA results are in general agreement with the values of the literature summary given in Meiksin & White (2004, table B1). However, we find approximately 0.03 less absorption at all redshifts. This is consistent with the fact that we have attempted to measure only the absorption due to the Ly$\alpha$ forest, while Meiksin & White (2004) gave values for all absorption in the Ly$\alpha$ forest region of a spectrum.

At $z = 2.2$, our results are also consistent with Schaye et al. (2003), who also attempted to measure only the absorption associated with the Ly$\alpha$ forest. They only removed metals absorption they could identify directly in the absorption spectra, so their removal completeness is unknown, and is probably a function of redshift. However, we find a shallower redshift evolution and less absorption at $z = 3.0$.

The best-fitting value of DA = 0.278 at $z = 3.0$ is lower than we expected to find when we started this work. In T04b and J05 we developed a concordance model of the Ly$\alpha$ forest at $z = 1.9$ – this model is referred to as model ‘A’ in T04b and J05. Model A uses a uniform UVB with the shape and redshift evolution due to Haardt & Madau (2001), and displayed graphically in Paschos & Norman (2005). Model A, while giving the measured value of DA at $z = 1.9$, predicts DA = 0.34 at $z = 3$. The clear implication is that there are more ionizing photons at $z = 3$ than predicted by Haardt & Madau (2001). J05 showed that the naive expectation that $\Gamma$ increases at $z = 3$ is nearly true. This value is a mean of 0.03 less absorption at all redshifts. However, we find a shallower redshift evolution and less absorption because we have fewer DA measurements giving a larger error on the measurement of the standard deviation of the DA values. We can subtract variances (squares of standard deviations) to estimate the variance of DA.

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