7 keV Sterile neutrino dark matter in $U(1)_{R}$-lepton number model

Sabyasachi Chakraborty, Dilip Kumar Ghosh and Sourov Roy

Department of Theoretical Physics, Indian Association for the Cultivation of Science, 2A & 2B Raja S.C.Mullick Road, Jadavpur, Kolkata 700 032, INDIA.

E-mail: tpsc3@iacs.res.in, tpdkg@iacs.res.in, tpsr@iacs.res.in

ABSTRACT: We study the phenomenology of a keV sterile neutrino in a supersymmetric model with $U(1)_{R}$-lepton number in the light of a very recent observation of an X-ray line signal at around 3.5 keV, detected in the X-ray spectra of Andromeda galaxy and various galaxy clusters including the Perseus galaxy cluster. This model not only provides a small tree level mass to one of the active neutrinos but also renders a suitable warm dark matter candidate in the form of a sterile neutrino with negligible active-sterile mixing. Light neutrino masses and mixing can be explained once one-loop radiative corrections are taken into account. The scalar sector of this model can accommodate a Higgs boson with a mass of $\sim 125$ GeV. In this model gravitino is the lightest supersymmetric particle (LSP) and we also study the cosmological implications of this light gravitino with mass $\sim O$(GeV).

KEYWORDS: Supersymmetry Phenomenology

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1 Introduction

We are living in an era enriched with many experimental breakthroughs and results especially in the area of astro-particle physics and cosmology. The most recent one is the identification of a weak line at \( E \sim 3.5 \) keV in the X-ray spectra of the Andromeda galaxy and many other galaxy clusters including the Perseus galaxy cluster, observed by XMM-Newton X-ray Space observatory\cite{1, 2}. The observed flux and the best fit energy peak are at

\[
\begin{align*}
\Phi_\gamma &= 4 \pm 0.8 \times 10^{-6} \ \text{photons cm}^{-2}\text{sec}^{-1}, \\
E_\gamma &= 3.57 \pm 0.02 \ \text{keV}.
\end{align*}
\]

(1.1)

Since atomic transitions in thermal plasma cannot account for this energy, therefore the concept of a dark matter, providing the possible explanation regarding the appearance of this photon line becomes extremely important. This result can be explained by a sterile neutrino \cite{3–8}, axion or axion like warm dark matter \cite{9–12}, axino \cite{13–15}, excited dark matter \cite{16, 17}, gravitino \cite{18, 19} and keV scale LSP \cite{20} as decaying dark matter. Other interesting scenarios with an annihilating scalar dark matter \cite{21}, decaying Majoron \cite{22} and a keV scale dark gaugino \cite{23} have also been considered in this context. In this work we consider sterile neutrino in a \( U(1)_R \)-lepton number model, which could provide a possible explanation for the emergence of the photon line. The observed flux and the peak of the energy readily translates to an active-sterile mixing in the range \( 2.2 \times 10^{-11} < \sin^2 2\theta_{14} < 2 \times 10^{-10} \) and the mass of the sterile neutrino dark matter \( M_N^R = 7.06 \pm 0.05 \) keV \cite{2}.

On the other hand, in high energy collider frontier two CERN based experiments ATLAS and CMS have confirmed the existence of a neutral elementary scalar boson of
nature, with mass around 125 GeV [24, 25]. Nevertheless, more analysis is required to confirm it as the Standard Model (SM) Higgs boson. In order to explain the mass of this scalar boson in a natural way, to address the question of nonzero neutrino mass and mixing and to provide a candidate for dark matter, many beyond standard model (BSM) theories have been pursued for quite some time and supersymmetry remains one of the most celebrated ones as of now. However, supersymmetric particle searches by ATLAS and CMS experiments for pp collision at center of mass energy 7 and 8 TeV, have observed no significant excess [26, 27] over the standard model background. This has put very stringent lower limits on the superpartner masses.

In the light of this present situation, $U(1)_{R}$-symmetric models with Dirac gauginos are well motivated because they can relax the strong bounds on the superpartner masses, explain the 125 GeV Higgs boson mass, provide non-zero neutrino mass at the tree as well as at the one loop level and can also accommodate a suitable dark matter candidate. Various aspects of different R-symmetric models have been studied and can be found in the literature [28–53]. In this work, we study a particular $U(1)_{R}$-symmetric model where we have identified the R-charges with lepton numbers in such a way that the lepton numbers of the standard model fermions correspond to the negative of their R-charges [48, 49]. The role of the down-type Higgs is played by the sneutrino since its vacuum expectation value (vev) is not constrained by the Majorana mass of the neutrino. The minimal extension of this model by adding a single right handed neutrino superfield also gives rise to very interesting phenomenological consequences [50]. It generates a tree level Dirac mass for one of the neutrinos in the R-symmetry preserving scenario. If R-symmetry is broken because of the presence of a non zero gravitino mass, then for small neutrino Yukawa coupling, $f \sim \mathcal{O}(10^{-4})$, the extended neutralino-neutrino mass matrix provides a sterile neutrino state accompanied by an active neutrino state. Here we identify the sterile neutrino as the warm dark matter in our model.

The presence of R-symmetry inhibits gauginos to acquire a Majorana mass. However, gauginos can have Dirac masses and to introduce the Dirac gaugino mass, one must consider a singlet chiral superfield $\hat{S}$, a triplet $\hat{T}$ and an octet $\hat{O}$ living in the adjoint representation of $U(1)_{Y}$, $SU(2)_{L}$ and $SU(3)_{C}$ respectively. The Dirac gaugino masses are also coined as ‘supersoft’ mass terms since they do not contribute to any logarithmic corrections to the scalar masses. The presence of Dirac gluino also helps to relax the bound on squark masses compared to MSSM and in addition flavor and CP violating constraints are suppressed in this class of models [35].

The plan of the paper is as follows. At first we describe the model in section II, with appropriate R-charge assignments. In section III we discuss very briefly, the scalar sector of the model and point out the extra contributions to the Higgs boson mass, which can arise both at the tree level as well as at the one loop level. Section IV addresses the issue of R-symmetry breaking and tree level Majorana masses of the sterile and one of the active neutrinos. Next in section V the essential features of the sterile neutrino as a keV warm dark matter candidate are discussed and its production mechanism and the dominant decay modes relevant to our model are highlighted. In section VI we briefly present a discussion related to the cosmology of the gravitino in this model with a few GeV mass and finally,
in section VII, we summarise our results.

2 U(1)_R-lepton number model with a right handed neutrino superfield

We study a U(1)_R-lepton number model, where in addition to the standard superfields of the MSSM - \( \hat{H}_u, \hat{H}_d, \hat{Q}_i, \hat{U}_i, \hat{D}_i, \hat{L}_i, \hat{E}_i \), this model includes a right handed neutrino superfield and a pair of vector-like SU(2)_L doublet superfields \( \hat{R}_u \) and \( \hat{R}_d \), with opposite hypercharge [50]. These two doublets carry non-zero R-charges (The R-charge assignments are given in Table I) and therefore, to avoid spontaneous R-breaking and the emergence of R-axions, they do not acquire any non-zero vev and would remain inert. R symmetry prohibits soft supersymmetry breaking terms like Majorana gaugino masses and trilinear scalar couplings. However, gauginos can acquire Dirac masses as mentioned in the introduction. The implications of adding a right-handed neutrino superfield \( \hat{N}_c \) is discussed later in detail. We would like to reiterate that the R-charge assignments are such that the lepton number of the SM fermions are negative of their corresponding R-charges.

| \( \hat{Q}_i \) | \( \hat{U}_i \) | \( \hat{D}_i \) | \( \hat{L}_i \) | \( \hat{E}_i \) | \( \hat{H}_u \) | \( \hat{H}_d \) | \( \hat{R}_u \) | \( \hat{R}_d \) | \( \hat{S} \) | \( \hat{T} \) | \( \hat{O} \) | \( \hat{N}_c \) |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| U(1)_R | 1 | 1 | 1 | 0 | 2 | 0 | 2 | 2 | 0 | 0 | 0 | 0 | 2 |

**Table 1.** U(1)_R charge assignments of the chiral superfields.

The generic superpotential, carrying R-charge of 2 units is

\[
W = y_{ij}^u \hat{H}_u \hat{Q}_i \hat{U}_j^c + \mu_u \hat{H}_u \hat{R}_d + f_i \hat{L}_i \hat{H}_u \hat{N}_c^c + \lambda_S \hat{S} \hat{H}_u \hat{R}_d + 2\lambda_T \hat{H}_u \hat{T} \hat{R}_d - M_R \hat{N}_c^c \hat{S} + \mu_d \hat{R}_u \hat{H}_d \\
+ \lambda_S \hat{S} \hat{R}_u \hat{H}_d + \frac{1}{2} \lambda_{ijk} \hat{L}_i \hat{L}_j \hat{E}_k^c + \lambda_{ijk}^\prime \hat{L}_i \hat{Q}_j \hat{D}_k^c + 2\lambda_T \hat{R}_u \hat{T} \hat{H}_d + y_{ij}^d \hat{H}_d \hat{Q}_i \hat{D}_j^c + y_{ij}^l \hat{H}_d \hat{L}_i \hat{E}_j^c \\
+ \lambda_N \hat{N}_c^c \hat{H}_u \hat{H}_d. \tag{2.1}
\]

Note that a subset (\( \lambda, \lambda' \)) of standard R-parity violating operators are present in the superpotential although the model is U(1)_R conserving (i.e. lepton number conserving). In a somewhat simplistic approach we have omitted the terms \( \hat{N}_c^c \hat{S} \hat{S} \) and \( \hat{N}_c \) from the superpotential.

In a realistic model one should also include supersymmetry breaking terms, such as the gaugino and scalar mass terms. The Dirac gaugino ‘supersoft’ mass terms are constructed from a spurion superfield \( W'_\alpha = \lambda_\alpha + \theta_\alpha D' \), if supersymmetry breaking is of the D-type. The Lagrangian containing the Dirac gaugino masses are [39, 40]

\[
\mathcal{L}_{\text{gaugino}}^{\text{Dirac}} = \int d^2\theta \frac{W'_\alpha}{\Lambda} [\sqrt{2}k_1 W_{1\alpha} \hat{S} + 2\sqrt{2}k_2 \text{tr}(W_{2\alpha} \hat{T}) + 2\sqrt{2}k_3 \text{tr}(W_{3\alpha} \hat{O})] + h.c. \tag{2.2}
\]

This D-term breaking generates Dirac mass for the gauginos, proportional to \( k_1 \frac{<D'_c>}{\Lambda} \), where \( \Lambda \) denotes the scale of SUSY breaking mediation. In a similar manner the U(1)_R conserving soft supersymmetry breaking terms in the scalar sector are generated by the spurion superfield \( \hat{X} \), defined as \( \hat{X} = x + \theta^2 F_X \). The non-zero vev of the F-term generates
the scalar soft terms as
\[
V_{\text{soft}} = m_H^2 H_u^\dagger H_u + m_{R_a}^2 R_a^\dagger R_a + m_{H_a}^2 H_a^\dagger H_a + m_{R_d}^2 R_d^\dagger R_d + m_{L_a}^2 L_a^\dagger L_a \\
+ m_{R_i}^2 R_i^\dagger R_i + M_N^2 \tilde{N}^c \tilde{N}^c + m_S^2 S^\dagger S + 2m_d^2 \text{tr}(T^\dagger T) + 2m_\Omega^2 \text{tr}(O^\dagger O) \\
+ (B\mu H_u H_d + \text{h.c.}) - (b\mu_L H_a \tilde{L}_i + \text{h.c.}) + (t_S S + \text{h.c.}) \\
+ \frac{1}{2} b_S(S^2 + \text{h.c.}) + b_T(\text{tr}(TT) + \text{h.c.}) + B_O(\text{tr}(OO) + \text{h.c.}).
\] (2.3)

The presence of the bilinear term \( b\mu_L H_a \tilde{L}_i \) in the soft supersymmetry breaking potential implies all the three left handed sneutrinos can acquire a non zero vevs \((v_i)\). To simplify, we perform a basis rotation as \( \tilde{L}_i = \frac{v_i}{v_a} \tilde{L}_a + e_{ib} \tilde{L}_b \) by which only one of the sneutrinos acquire a non zero vev \((v_a)\) and we choose it to be the electron sneutrino \((a = 1(e))\). We also choose the neutrino Yukawa coupling \((f)\) in such a manner that only \( \tilde{L}_a \) couples with \( \tilde{N}^c \), the right-handed neutrino superfield \([50]\). Finally, we choose a very large \( \mu_d \) such that the superfields \( H_d \) and \( \tilde{R}_a \) gets decoupled, which also implies that the left handed electron type sneutrino now plays the role of a down type Higgs field. We would like to emphasise that the model is lepton number conserving and therefore, the sneutrino vev is not constrained from the Majorana mass of the neutrinos. This is clearly different from the standard R-parity violating scenario.

In the mass eigenstate basis (primed superfields) of the down-type quarks and the charged leptons\(^1\) the superpotential takes the following form \([50]\)

\[
W = y_{ij}^e H_a \tilde{Q}_i \tilde{U}_j^c + \mu_a H_u \tilde{R}_d + f \tilde{L}_a H_u \tilde{N}^c + \lambda_S \tilde{S} H_u \tilde{R}_d + 2\lambda_T H_u \tilde{T} \tilde{R}_d - M_R \tilde{N}^c \tilde{S} + W',
\] (2.4)

and
\[
W' = \sum_{b=2,3} f_b^L \tilde{L}_a^b \tilde{L}_b^c + \sum_{k=1,2,3} f_k^L \tilde{L}_a^k \tilde{Q}_k^c \tilde{D}_k^c + \sum_{k=1,2,3} \frac{1}{2} \tilde{\chi}_{23k} \tilde{E}_2^k \tilde{E}_3^c \]

\[+ \sum_{j,k=1,2,3,b=2,3} \tilde{\lambda}_{bjk} \tilde{L}_b^j \tilde{Q}_j^c \tilde{D}_k^c. \] (2.5)

In our subsequent analysis we stay in this mass basis but remove the prime from the fields and make the replacement \( \tilde{\lambda}, \tilde{\chi} \rightarrow \lambda, \chi \). The soft supersymmetry breaking but \( U(1)_R \) preserving terms in the rotated basis are

\[
V_{\text{soft}} = m_H^2 H_u^\dagger H_u + m_{R_a}^2 R_a^\dagger R_a + m_{H_a}^2 H_a^\dagger H_a + m_{R_d}^2 R_d^\dagger R_d + m_{L_a}^2 L_a^\dagger L_a \\
+ m_{R_i}^2 R_i^\dagger R_i + M_N^2 \tilde{N}^c \tilde{N}^c + m_S^2 S^\dagger S + 2m_d^2 \text{tr}(T^\dagger T) + 2m_\Omega^2 \text{tr}(O^\dagger O) \\
+ (B\mu H_u H_d + \text{h.c.}) - (b\mu L H_a \tilde{L}_i + \text{h.c.}) + (t_S S + \text{h.c.}) \\
+ \frac{1}{2} b_S(S^2 + \text{h.c.}) + b_T(\text{tr}(TT) + \text{h.c.}) + B_O(\text{tr}(OO) + \text{h.c.}).
\] (2.6)

\(^1\) Note that the mass of the charged lepton of flavor \( a \) can come from R-symmetry preserving supersymmetry breaking operators \([48]\).
In the R-symmetric case, the lightest eigenvalue of the neutralino mass matrix, written in the basis \( (\tilde{b}^0, \tilde{u}^0, \tilde{R}_d^0, N^c) \) and \( (\tilde{S}, \tilde{T}^0, \tilde{H}_d^0, \nu_e) \), provides a tree level Dirac neutrino mass, which can be written as [50]

\[
m_{\nu_e}^D = \frac{v^3 \sin \beta g f \lambda_T}{\sqrt{2} \gamma M_D^2 M_2^D} (M_2^D - M_1^D),
\]

where \( M_1^D, M_2^D \) stands for Dirac bino and wino masses respectively, \( \gamma = \mu_u + \lambda_S v_S + \lambda_T v_T \), \( g \) is the \( SU(2) \) gauge coupling, \( \tan \beta = \frac{v_u}{v_a} \), \( v \equiv \sqrt{v_u^2 + v_a^2} = \frac{\sqrt{2} M_W}{g} \). To obtain this particular form in eq. (2.7) we have assumed certain relations involving the parameters and they are

\[
\lambda_T = \tan \theta_W \lambda_S,
M_R = \frac{\sqrt{2} f M_D^2 \tan \beta}{g \tan \theta_W}.
\]

Therefore, with appropriate choice of parameters one can easily obtain a small tree level Dirac neutrino mass \( \sim 0.1 \text{ eV} \).

3 Scalar sector

In this section we shall mention very briefly about the scalar sector of this particular model. For a detailed discussion we refer the reader to [50]. The lightest CP even scalar mass matrix, in the basis of \( (H_u, \tilde{\nu}, S, T) \), provide the CP even Higgs boson. It is remarkable that the neutrino Yukawa coupling \( f \) renders a tree level correction to the lightest Higgs boson mass, which we calculate as

\[
M_h^2 \leq M_t^2 \cos^2 2\beta + f^2 v^2 \sin^2 2\beta.
\]

For \( f \sim \mathcal{O}(1) \) and for small \( \tan \beta \), the tree level Higgs boson mass can satisfy the present observed value, close to 125 GeV [50]. It is also pertinent to mention that the singlet and the triplet fields provide very important loop corrections to the Higgs boson mass. These contributions can be sizable if the singlet and the triplet couplings \( \lambda_S \) and \( \lambda_T \) are large. The dominant radiative corrections to the quartic potential can be written as [54],

\[
\delta \lambda_{\alpha} = \frac{3g_\alpha^4}{16\pi^2} \ln \left( \frac{m_{\alpha}^2}{m_t^2} \right) + \frac{5\lambda_T^4}{16\pi^2} \ln \left( \frac{m_T^2}{v^2} \right) + \frac{\lambda_S^4}{16\pi^2} \ln \left( \frac{m_S^2}{v^2} \right) - \frac{1}{16\pi^2} \frac{\lambda_T^2 \lambda_S^2}{m_T^2 - m_S^2} \left( m_T^2 \left\{ \ln \left( \frac{m_T^2}{v^2} \right) - 1 \right\} - m_S^2 \left\{ \ln \left( \frac{m_S^2}{v^2} \right) - 1 \right\} \right),
\]

\( \delta \lambda_{\nu} = \frac{3g_\nu^4}{16\pi^2} \ln \left( \frac{m_{\nu}^2}{m_b^2} \right) + \frac{5\lambda_T^4}{16\pi^2} \ln \left( \frac{m_T^2}{v^2} \right) + \frac{\lambda_S^4}{16\pi^2} \ln \left( \frac{m_S^2}{v^2} \right) - \frac{1}{16\pi^2} \frac{\lambda_T^2 \lambda_S^2}{m_T^2 - m_S^2} \left( m_T^2 \left\{ \ln \left( \frac{m_T^2}{v^2} \right) - 1 \right\} - m_S^2 \left\{ \ln \left( \frac{m_S^2}{v^2} \right) - 1 \right\} \right),
\]

(3.3)

\( ^2 \)In this paper we shall not explore such a possibility and concentrate on the region of parameter space where \( f \sim \mathcal{O}(10^{-4}) \), which produces a keV sterile neutrino state.
and finally,

\[\delta \lambda_3 = \frac{5 \lambda_T^4}{32 \pi^2} \ln \left( \frac{m_T^2}{v^2} \right) + \frac{1}{32 \pi^2} \lambda_S^4 \ln \left( \frac{m_S^2}{v^2} \right) + \frac{1}{32 \pi^2} \lambda_T^2 \lambda_S^2 \left( \frac{m_T^2}{m_S^2} - 1 \right) \ln \left( \frac{m_T^2}{m_S^2} \right) - 1 \}

(3.4)

Therefore, for large \( \lambda_S, \lambda_T \sim O(1) \), a 125 GeV Higgs boson mass can easily be accommodated in this model even in the presence of a light stop mass and negligible left-right mixing.

4 R-symmetry breaking

Until now we have constrained ourselves in the R-symmetry preserving scenario. Although the R-symmetric case in this regard is interesting and should be explored in much more detail but in our work we pursue the path, where R-symmetry is broken. Recent cosmological observations point towards a vanishingly small vacuum energy or cosmological constant associated with our universe. Spontaneously broken supergravity theory in a hidden sector requires a non zero value of the superpotential in vacuum in order to have this small vacuum energy. As the superpotential carries R-charge of two units \([R[W] = 2]\), therefore R-symmetry is broken when the superpotential acquires a non zero vev \( \langle W \rangle \). Furthermore, a non zero gravitino mass also requires a non zero \( \langle W \rangle \), thereby one can consider the gravitino mass as the order parameter of R-symmetry breaking.

The breaking of R-symmetry has to be communicated to the visible sector and in this context we confine ourselves to the case of anomaly mediation, which plays the role of the messenger of R-symmetry breaking [48, 50]. Such a scenario generates very small (\( \sim \) a few MeV) Majorana gaugino masses and trilinear scalar couplings, \( M_i \sim \frac{g'^i}{16 \pi^2} m_{3/2} \) and \( A_{u/d} = \frac{\tilde{b}_{u/d} v_{u/d}}{16 \pi^2 m_{u/d}} m_{3/2} \) [55, 56], as long as the gravitino mass is in the range of a few GeV.

In the R-breaking case, the neutralino mass matrix written in the basis \( (\tilde{b}^0, \tilde{S}, \tilde{w}^0, \tilde{T}, \tilde{H}_u^0, N^c, \nu_e) \), is given by

\[
M^M_{\chi} = \begin{pmatrix}
M_1 & M_1^D & 0 & 0 & 0 & \frac{g' v_u}{\sqrt{2}} & 0 & -\frac{g' v_u}{\sqrt{2}} \\
M_1^D & 0 & M_2 & M_2^D & 0 & \lambda_S v_u & 0 & M_R \\
0 & 0 & M_2 & M_2^D & 0 & 0 & \lambda_T v_u & 0 \\
0 & \lambda_S v_u & 0 & \lambda_T v_u & 0 & \mu_u + \lambda_S v_S + \lambda_T v_T & 0 & 0 \\
\frac{g' v_u}{\sqrt{2}} & 0 & -\frac{g' v_u}{\sqrt{2}} & 0 & \mu_u + \lambda_S v_S + \lambda_T v_T & 0 & -f v_a & 0 \\
0 & M_R & 0 & 0 & 0 & 0 & -f v_a & 0 \\
-\frac{g' v_u}{\sqrt{2}} & 0 & 0 & 0 & 0 & -f v_a & 0 & 0 \\
\end{pmatrix}
\]

(4.1)
An approximate expression for the tree level Majorana neutrino mass is given by [50]

\[(m_\nu)_{\text{Tree}} \simeq -v^2 \left[ g \lambda_T v^2 (M_2^D - M_1^D) \sin \beta \right] \frac{1}{[M_1 G^2 + M_2 \delta^2]} , \]  

(4.2)

where

\[\begin{align*}
\alpha &= \frac{2 M_1^D M_2^D \gamma \tan \beta}{g \tan \theta_w} + \sqrt{2} v^2 \lambda_S \tan \beta (M_1^D \sin^2 \beta + M_2^D \cos^2 \beta), \\
\delta &= \sqrt{2} M_1^D v^2 \lambda_T \tan \beta ,
\end{align*}\]

(4.3)

and \(\gamma\) has been defined earlier. Note that the neutrino Yukawa coupling \(f\) does not arise in this expression because of our choice in eq. (2.8). Therefore, it is obvious from eq. (4.2) that in order to obtain a small tree level Majorana neutrino mass, we either require a small \(\lambda_T\) or nearly degenerate Dirac gaugino masses\(^3\). In this work we are interested in the sterile neutrino which might play the role of keV dark matter. From the \(8 \times 8\) neutralino mass matrix, the sterile neutrino mass can be approximated as

\[M_N^R \simeq M_1^2 \frac{2 f^2 \tan^2 \beta}{g^2} . \]  

(4.4)

For a wide range of parameters the active-sterile mixing can also be estimated as

\[\theta_{14}^2 \simeq \frac{(m_\nu)_{\text{Tree}}}{M_N^R} . \]  

(4.5)

In figure (1), we show in the \((f - \tan \beta)\) plane the contour of sterile neutrino mass fixed at 7.06 keV and also two different contours of \(\sin^2 2 \theta_{14}\), fixed at the lower and upper limit at \(2.2 \times 10^{-11}\) and \(2 \times 10^{-10}\) respectively. We have chosen the gravitino mass, \(m_{3/2}\) to be 10 GeV and \(M_1^D = 900\) GeV, keeping a degeneracy between the Dirac gaugino masses, \(\epsilon \equiv (M_2^D - M_1^D) = 10^{-4}\) GeV. We have also fixed \(\mu_u = 750\) GeV, \(\lambda_S = 1.1\), \(v_S = -0.1\) GeV and \(v_T = 0.1\) GeV.

The sterile neutrino mass contour can be easily explained by looking at eq. (4.4). Similarly from eq. (4.2), eq. (4.4) and eq. (4.5), it is straightforward to show that \(\sin^2 2 \theta_{14}\) goes as \(\frac{1}{1+\tan^2 \beta}\). This means that for smaller \(\tan \beta\) one would expect larger mixing angle for fixed values of other parameters. This is also evident from figure 1. Furthermore, for larger Dirac gaugino masses, the active neutrino mass gets reduced (see eq. (4.2)), which also implies a reduction in the active-sterile mixing.

Looking at figure 1, we observe that the largest value of the active-sterile mixing, required to explain the observed photon line flux at an energy \(E \approx 3.5\) keV, corresponds to the minimum value of \(\tan \beta\). In fact, for this particular case shown in figure 1, \((\tan \beta)_{\text{min}} \approx 11.3\). Similarly the smallest active-sterile mixing \((\sin^2 2 \theta_{14} = 2.2 \times 10^{-11})\) provides the maximum allowed value of \(\tan \beta\), which in this case turns out to be \((\tan \beta)_{\text{max}} \approx 33\). In order to obtain an analytical relationship between the lower limit of \(\tan \beta\) and \(M_1^D\), we can

\(^3\)A detailed discussion on how to fit the light neutrino masses and mixing in this model can be found in [50].
Figure 1. The contour in the black thick line represents a sterile neutrino mass of 7 keV. Contours in red (dotted) and blue (dashed) colours show active-sterile mixing $2.2 \times 10^{-11}$ and $2 \times 10^{-10}$ respectively.

solve for $\tan \beta$ using eq. (4.5), with $\sin^2 2\theta_{14} = 2 \times 10^{-10}$ and $M_{N}^R = 7.06$ keV. This gives rise to

$$(\tan^2 \beta)_{\text{min}} = \frac{4v^2 \{g\lambda_T v^2 (M_2^D - M_1^D)\}^2}{(1.4 \times 10^{-15} \text{ GeV})[M_1 \alpha'^2 + M_2 \delta'^2]} - 1,$$  

(4.6)

where

$$\alpha' \simeq \frac{2(M_2^D)^2\mu_u}{g'} + \sqrt{2}v^2 \lambda_s M_2^D,$$

$$\delta' \simeq \sqrt{2} M_2^D v^2 \lambda_T.$$  

(4.7)

In a similar way an analytical expression for the upper limit of $\tan \beta$ can also be derived.

Figure 2 shows the lower and upper limits of $\tan \beta$ as a function of $M_2^D$, for $\mu_u = 700$ GeV, $m_{3/2} = 10$ GeV and $\epsilon = 10^{-4}$ GeV. We have fixed $\lambda_S$ at the previously mentioned value. The horizontal grey line shows the upper limit on $\tan \beta$ arising from the contribution of the leptonic Yukawa coupling, $f_\tau \equiv \lambda_{133}$ to the ratio $R_\tau \equiv \frac{\Gamma(\tau \rightarrow e\bar{\nu}_e\nu_\tau)}{\Gamma(\tau \rightarrow \mu\bar{\nu}_\mu\nu_\tau)}$. The resulting constraint is $f_\tau < 0.07 \left( \frac{m_{\tilde{\tau}_R}}{100 \text{ GeV}} \right)$ [48] and considering stau mass, close to 280 GeV, translates into an upper limit on $\tan \beta \approx 19$. For higher stau mass this upper limit on $\tan \beta$ gets relaxed. The blue dashed line shows the lower bound on $\tan \beta$, as a function of $M_2^D$, arising from the precision measurements of the deviations in the couplings of the $Z$ boson to charged leptons [48].
Figure 2. Showing the lower and upper limits of $\tan \beta$ from X-ray analysis as a function of $M_2^D$ for $\mu_u = 700$ GeV, $m_{3/2} = 10$ GeV and $\epsilon = 10^{-4}$ GeV.

We infer from the above discussions, that in a large region of the parameter space, the lower limit on $\tan \beta$, satisfying the estimated mass and mixing of the sterile neutrino dark matter particle coming from the recent observation of an X-ray line signal at energy 3.5 keV is stronger than the lower limit on $\tan \beta$ coming from the electroweak precision measurements. On the other hand, the upper limit on $\tan \beta$ coming from the X-ray observations becomes stronger than the upper limit arising from the $\tau$ Yukawa coupling contribution to $R_\tau$ only for higher values of $M_2^D$ as shown in figure 2 for specific choices of $\mu_u$ and $m_{3/2}$. Combining these lower and upper limits on $\tan \beta$ from X-ray observations and measurement of $R_\tau$, we can find a range of $M_2^D$ that is allowed. For smaller values of $\mu_u$ and $m_{3/2}$, the upper and lower limits of $M_2^D$ shift to higher values (see eq. (4.6)).

We also observe from figure 1 that the allowed values of $f$ is of the order of $10^{-4}$. Such a small value of $f$, implies negligible extra contribution to the tree level Higgs boson mass. Therefore, to elevate the Higgs boson mass to 125 GeV, we have to rely on the loop corrections. Sizable radiative corrections are obtained if $\lambda_S, \lambda_T$ are large ($\mathcal{O}(1)$) and this would imply nearly degenerate Dirac gaugino masses ($\epsilon \sim 10^{-4}$ GeV) in order to have the active-sterile mixing $\sin^2 2\theta_{14} \sim 10^{-11}$ and a tree level active neutrino mass $\lesssim 0.05$ eV. The other case, which can relax this strong degeneracy between Dirac gaugino masses, corresponds to the case of small $\lambda_S, \lambda_T \sim \mathcal{O}(10^{-4})$, which implies multi-TeV stop to fit the Higgs boson mass. Therefore, this model provides a very interesting possibility where we can connect the Higgs sector with the neutrino sector (both active as well as sterile neutrino).
5 Right handed neutrino as a keV warm dark matter

To accommodate sterile neutrino as a warm dark matter candidate, it is very important to make sure that the active sterile mixing is very small \cite{57-62} and within the valid range of different X-ray experiments. A rough bound on the active-sterile mixing can be parametrised as \cite{63}

\[
\theta_{14}^2 \leq 1.8 \times 10^{-5} \left( \frac{1 \text{keV}}{M_{R}^N} \right)^5.
\]

(5.1)

Along with the strict bound coming from different X-ray experiments, the keV sterile neutrino must produce the correct relic density \( \Omega_N h^2 \sim 0.1 \), in order to identify itself with the warm dark matter. An approximate formula for the relic density of sterile neutrinos, produced in the early universe with negligible lepton asymmetry via non-resonant oscillations with active neutrinos, known as the Dodelson-Widrow (DW) mechanism \cite{64} can be written as \cite{65}

\[
\Omega_N h^2 \sim 0.3 \left( \frac{\sin^2 2\theta_{14}}{10^{-10}} \right) \left( \frac{M_{R}^N}{100 \text{ keV}} \right)^2,
\]

(5.2)

where \( \Omega_N \) is the ratio of the sterile neutrino density to the critical density of the Universe and \( h = 0.673 \).

Different experimental observations have also put lower limits on the mass of the keV warm dark matter. A very robust bound for fermionic dark matter particles comes from Pauli exclusion principle. By claiming the maximal (Fermi) velocity of the degenerate fermionic gas in the dwarf spheroidal galaxies is less compared to the escape velocity, translates into a lower bound on the sterile neutrino dark matter mass, i.e \( M_{R}^N > 0.41 \text{ keV} \) \cite{66, 67}. Model dependent bounds on the mass of the warm dark matter are much more stringent and obtained from analysing Lyman-\( \alpha \) experiment \cite{68, 69}.

In figure 3 we present a scatter plot by scanning the parameter space of our model and also show the compatibility of those points with the current experimental findings. The red circles are the points obtained by varying the parameters as \( 500 \text{ GeV} < M_1^D < 1.2 \text{ TeV}, \ 10^{-5} < f < 10^{-3}, \ 2.7 < \tan \beta < 17, \ 400 \text{ GeV} < m_{\tilde{t}_1, \tilde{t}_2} < 1.2 \text{ TeV}, \) keeping \( \epsilon \equiv (M_2^D - M_1^D) \sim 10^{-4} \text{ GeV} \). \( \mu_u \) and \( \lambda_S \) are fixed at \( 750 \text{ GeV} \) and 1.1 respectively (\( \lambda_T = \lambda_S \tan \theta_W \sim 0.6 \)). All these points respect a Higgs boson mass in between 124.4 GeV and 126.2 GeV avoiding any tachyonic scalar states.

Similar plot can also be generated where \( \lambda_T \sim 10^{-5} \). Therefore, to fit the Higgs boson mass in that case, one requires \( m_\tilde{t} > 5 \text{ TeV} \). However, the degeneracy between \( M_1^D \) and \( M_2^D \) is somewhat lifted where \( \epsilon \gtrsim 1 \text{ GeV} \).

The horizontal yellow band in figure 3 is ruled out by the Tremaine Gunn bound, which implies \( M_{R}^N < 0.4 \text{ keV} \) \cite{66, 67}. The blue region is excluded by taking into consideration the diffuse X-ray background \cite{70}. Cluster X-ray bound rules out a region in the mass-mixing plane by taking into consideration XMM-Newton observations from the Coma and Virgo clusters \cite{71}. Constraints from the cosmic X-ray background (CXB) rules out the region in red stripes \cite{70}. Chandra observation of M31 \cite{72} rules out the region in grey. The light
blue line corresponds to the correct relic density provided by the sterile neutrino warm dark matter via DW mechanism. The light blue region above this line marked as DW is ruled out because of the over abundance of sterile neutrino dark matter. The horizontal and vertical lines show the region in the mass and mixing plane consistent with the observed 3.5 keV X-ray line with more than 3σ significance. The black star corresponds to the best fit point. It is clearly evident from this figure that such a small mixing is completely in conflict with the DW production mechanism of sterile neutrinos. However, resonant production of sterile neutrinos in the presence of a lepton asymmetry in primordial plasma can be very important and produce correct relic abundance of the keV sterile neutrinos [65, 73]. Recent studies have shown that a cosmological lepton asymmetry $L \sim O(10^{-3})$ is capable of producing correct relic density of 0.119 [4]. It was shown in [74–81] that active-sterile neutrino oscillations can themselves create a cosmological lepton number of this magnitude, assuming that the number of sterile neutrinos is negligible to start with. Such a possibility can be easily conceived in our model to generate a large lepton asymmetry.

Let us note in passing that sterile neutrino production in non-standard cosmology with
low reheating temperature (\(\sim\) a few MeV) has also been discussed in the literature [82–84]. If the universe has undergone inflation and was never reheated to a temperature above a few MeV then the relic abundance of the sterile neutrinos can be written as
\[
\Omega_N h^2 = 10^{-7} d_\alpha \left( \frac{\sin^2 2\theta_{14}}{10^{-10}} \right) \left( \frac{M_N^R}{10 \text{ keV}} \right) \left( \frac{T_R}{5 \text{ MeV}} \right)^3,
\]
where \(d_\alpha = 1.13\), assuming that the sterile neutrino couples only with \(\nu_e\) as in our case. It is obvious from the above expression that for allowed values of \(\sin^2 2\theta_{14}\) and \(M_N^R\) (from the recent X-ray observation) this production mechanism will give rise to severe under abundance of sterile neutrinos.

In our model sterile neutrinos can also be produced non-thermally via the decay of heavier scalar particles. However, a quantitative estimate of the relic density requires a thorough investigation and we postpone the discussion of this method of production for a future work [85].

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure4.png}
\caption{The plot shows the sterile neutrino lifetime as a function of the sterile neutrino mass. The black vertical line represents the 7 keV mass of the sterile neutrino. The red points represent the total lifetime of the sterile neutrino.}
\end{figure}

**5.1 Sterile neutrino decay**

The most dominant decay mode of the sterile neutrino is \(N \rightarrow 3\nu\). The corresponding decay rate for this process is given by [57]
\[
\Gamma_{3\nu} = 8.7 \times 10^{-31} \text{ sec}^{-1} \left( \frac{\sin^2 2\theta_{14}}{10^{-10}} \right) \left( \frac{M_N^R}{1 \text{ keV}} \right)^5.
\]

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The principal radiative decay mode of the sterile neutrino which is of concern here is \( N \to \nu \gamma \) and the decay width is

\[
\Gamma_{\nu \gamma} = 1.38 \times 10^{-32} \text{ sec}^{-1} \left( \frac{\sin^2 2\theta_{14}}{10^{-10}} \right) \left( \frac{M_R}{1 \text{ keV}} \right)^5.
\]  

(5.5)

This decay produces a monochromatic photon line at \( E_\gamma = \frac{M_R}{2} \). From figure (4) we can see that the lifetime of the sterile neutrino is much larger than the age of the universe.

\section{Gravitino cosmology}

As mentioned earlier, the gravitino mass is the order parameter of R-breaking. If the mass is around a few GeV, it can be a candidate for cold dark matter \[86\]. In our scenario, the gravitino is an unstable particle and decays to an active/sterile neutrino and a monochromatic photon. The tree level decay mode into an active neutrino final state \( \tilde{G} \to \gamma \nu_e \) is suppressed by the very small mixing \( U_{\tilde{b}\nu_e} \sim 10^{-7} \) between the bino and active neutrino \( \nu_e \). \[87\]. Interestingly, in our model the most dominant decay mode of gravitino is into a photon and a sterile neutrino \( \tilde{G} \to N \gamma \) and the decay width is given as

\[
\Gamma_{\tilde{G} \to N \gamma} \sim \frac{|U_{\tilde{b}N}|^2 m_3^{3/2}}{32\pi M_F^2},
\]  

(6.1)

where \( U_{\tilde{b}N} \) is the bino sterile neutrino mixing angle. Because of the presence of the term \( M_R \hat{N} \hat{S} \) in the superpotential and the bino Dirac mass term in the Lagrangian, the tree level bino sterile neutrino mixing is not strongly suppressed \( \sim 10^{-2} \).

For the sake of completeness, let us mention that at the one loop level the decay \( \tilde{G} \to \gamma \nu_e \) occurs \[88-91\] via trilinear R-parity violating coupling \( \lambda_{133} \) which we have identified with the bottom Yukawa coupling. We have checked that this process is also suppressed compared to the tree level decay \( \tilde{G} \to N \gamma \). The one-loop contribution to the decay \( \tilde{G} \to N \gamma \) is negligible because of small active-sterile mixing.

Taking into account the most dominant decay mode of the gravitino in the sterile neutrino plus photon final state, for a 10 GeV gravitino mass, the lifetime is close to \( 10^{15} \) sec. Therefore, to satisfy the experimental constraints coming from the diffuse photon background, one has to consider a scenario where the gravitino density is very much diluted. In order to provide a quantitative analysis we note that for a gravitino of mass 10 GeV the limit on the diffuse photon flux is around \( 6.89 \times 10^{-7} \text{GeV cm}^{-2} \text{sec}^{-1} \). \[92\]. This can be translated into a bound on the gravitino relic density and we find

\[
\Omega_{3/2} h^2 < 4.34 \times 10^{-13} \left( \frac{10^{-2}}{U_{\tilde{b}N}} \right)^2,
\]  

(6.2)

for a 10 GeV gravitino. Note that this bound depends strongly on the mass of the gravitino and will get relaxed for a smaller gravitino mass. To satisfy such a strong bound on the gravitino relic density, one must account for a very low reheating temperature. If the reheating temperature is above the SUSY scale, the gravitino relic density would be too large \[93\]. Therefore, the reheating temperature must lie much below the SUSY threshold.
Following [43], we see that if the reheating temperature is below the SUSY threshold, the gravitinos are produced by thermal scattering with neutrinos and bottom quarks. Using the results of [43] for production of gravitinos, we obtain an upper bound on the reheating temperature for a 10 GeV gravitino as

\[ T_R < 127 \left( \frac{v_a}{30 \text{GeV}} \right)^{2/7} \left( \frac{m_b}{500 \text{GeV}} \right)^{4/7} \left( \frac{10^{-2}}{U_{bN}} \right)^{2/7} \text{GeV}. \] (6.3)

Such a low reheating temperature might have important implications in the context of different baryogenesis and leptogenesis scenarios.

7 Conclusion

Recent observation of a weak X-ray line around \( E_\gamma = 3.5 \) keV by XMM-Newton telescope coming from Andromeda galaxy and various galaxy clusters have been studied in the light of a \( U(1)_R \)-lepton number model, with a single right handed neutrino. We have shown explicitly that a sterile neutrino of mass about 7 keV and with appropriate active-sterile mixing can easily be obtained in our model. We briefly mention different production mechanisms of the sterile neutrino.

Allowed ranges of the mass and mixing helped us to put bounds on \( \tan \beta \) as a function of the Dirac wino mass \( M_D^2 \). Combining these bounds with the limits coming from the measurements of the \( \tau \) Yukawa coupling contribution to the ratio \( R_\tau \equiv \Gamma(\tau \to e\bar{\nu}_e\nu_\tau)/\Gamma(\tau \to \mu\bar{\nu}_\mu\nu_\tau) \), one obtains strong upper and lower bounds on \( M_D^2 \).

In addition, we have also discussed the Higgs sector briefly and pointed out different possibilities to have a Higgs boson mass around 125 GeV. Finally, gravitino is the LSP in our model with a mass about a few GeV and gravitino mass is the order parameter of \( R \)-symmetry breaking. The gravitino can decay into a photon plus active or sterile neutrino. Therefore, we have also presented a short discussion on the cosmological implications of the gravitino. We have taken into account the most robust constraint coming from the diffuse photon background, which readily puts a very stringent bound on the gravitino relic density. This eventually imposes an upper limit (\( \lesssim 130 \) GeV) on the reheating temperature of the universe.

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