Radiation Dosimetry of Binary Pulsars

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Abstract

Companion stars exposed to high energy radiation from a primary neutron star or accreting black hole can experience significant spallation of their heavy elements, so that their atmospheres would be extremely rich in lithium, beryllium, and especially boron. In this paper we note that the detection or non-detection of these elements, and their relative abundances if detected, would provide a diagnostic of the high energy output of the primary, and possibly the shock acceleration of particles at the companion’s bow shock in a pulsar wind.

Keywords: Pulsars: general; Ultraviolet : stars; Physical processes: abundances.

1. Introduction

Pulsar emission theory is by now an established if unresolved topic. Radio pulsations are believed to imply counterstreaming pairs, which are produced via the curvature radiation of very high energy gamma rays. Below the “death line”, it is believed that the primary radiation is mainly curvature radiation that fails to develop a next generation of pairs. Even while pulsing, a pulsar could easily put out $\sim 10^{-3}$ of its spin down energy into pulsed gamma rays, (Usov 1983) since a) pair production shorts out the field to the point that the pairs are accelerated only enough to marginally produce pairs, and b)
charged particles that are accelerated outward will eventually reach a site where emitted photons can escape without further pair production. A reasonable estimate for curvature radiation is probably the product of the Goldreich-Julian current and the polar voltage drop, whence the fraction of total spin down power radiated as curvature gamma rays can be of order $10^{-3}$ or more for millisecond pulsars. Luminous, nearby pulsars such as the Crab are observed to yield pulsed gamma rays at a total power consistent with theoretical expectations. Recent EGRET limits are also consistent with these expectations (Fierro et al. 1995). However, additional gamma radiation may be generated by pairs striking and cascading in the atmospheres of companions to pulsars. Also, the pair luminosity itself may be enhanced by shock acceleration of pulsar wind particles at the bow shock of its companion (Arons and Tavani, 1994, Grove et al. 1995).

In this paper, we suggest that the output in high energy ($E > 20$ Mev) quanta from pulsars with close binary companions can be diagnosed via the production of light elements in the companion’s atmosphere by photospallation. The idea of using light elements as a dosimetric diagnostic of pulsars is not new: it has been discussed in the context of very young pulsars irradiating early supernova remnants (Eichler and Letaw 1987). More recently, Li has been reported to be present in roughly cosmic abundances in V404 Cygni, contrary to expectations that it should have been mostly destroyed. It has been considered that the Li has been replenished by photospallation caused by irradiation from its compact (primary) companion. Although this invokes some numerical coincidence, alternative explanations for the Li abundance in V404 Cygni-like systems are briefly mentioned below.

The question of whether “black widow” type evaporation scenarios occur for accreting neutron stars and pulsars is still an open one. It has been suggested that heat induced evaporation can be important for companions to both accreting neutron stars and pulsars (Eichler and Ko 1988; Ruderman et al. 1989; Ruderman, Shaham and Tavani 1989) though the efficiency of mass loss and extent of ablation have been questioned on both observational and theoretical grounds (Levinson and Eichler 1991; Eichler 1991; Gedalin and Eichler 1993). This matter is particularly questionable for low luminosity pulsars where some mechanism must be invoked for converting the spin down power to a form of energy suitable for mass evaporation. In the latter case, some scenarios assume that the pulsar spin down power is somehow converted to soft gamma rays with high efficiency (Kluzniak et al. 1988; Phinney et al. 1988). Several eclipsing pulsars have been discovered at this time (Fruchter et al. 1988; Lyne et al. 1990; Johnston et al. 1992) and the eclipse is suggestive of some mass loss mechanism, though not necessarily implicative of significant ablation.
In the PSR 1957+20 system, for example, viable eclipse mechanisms typically require a plasma frequency at the eclipse site of about 0.1 of the frequency of the radio waves that are being eclipsed (Gedalin and Eichler 1993). Assuming that the outflow proceeds at about the orbital velocity or somewhat higher, this implies a mass loss rate of about $10^{13} \text{g/s}$.

2. Photospallation and light elements

The photospallation cross section for $^{12}\text{C} + \gamma \rightarrow ^{11}\text{B} + p$ becomes significant at photon energies above 15 MeV or so. It averages about 5 millibarns in the photon energy range 20 to 25 MeV, or about 1 millibarn per unit logarithm in photon energy at 20 MeV (Taran and Gorbunov 1967). Higher energy gamma rays or pairs hitting the companion surface cascade via bremsstrahlung pair production cycles, and always pass through this energy range. Shock acceleration of pairs followed by synchrotron emission would convert much of the shock energy to photons of about several MeV, so the amount of photospallation predicted by this scenario depends sensitively on a detailed calculation of the synchrotron spectrum.

We consider the consequences of the hypothesis that some fraction $\epsilon$ of the pulsar’s spin down power $L$ arrives in the form of (or is converted to) 20 Mev photons. For convenience, assume the average photon energy included in this fraction is $10^{-5}$ erg. Then the hard photon flux incident on the companion is $f = 3 \times 10^{14} f_{14.5}$, where $f_{14.5} = (\frac{\epsilon}{3 \times 10^{-5}}) L_{35} D_{11}^{-2}$ photons/cm$^2$ s, $L_{35}$ is $L$ in units of $10^{35}$ erg s$^{-1}$, and $D_{11}$ is the orbital separation in units of $10^{11}$ cm. The lifetime of a carbon nucleus exposed to $f$ is about $3 \times 10^{12} / f_{14.5}$ seconds.

Can the top radiation length of material remain on the surface for more than $10^{10}$ seconds (in which case the heavy elements would be completely destroyed)? The mass loss rate for the PSR 1957+20 system is conservatively estimated to be of order $10^{12} \text{g/s}$, and could easily be $10^{13} \text{g/s}$ (so we define it to be $\dot{M}_{13}$ times this amount), from a surface area of $16\pi R_2^2 \times 10^{20} \text{cm}^2$, (here $R_2$ is the radius in units of $2 \times 10^{10}$ cm. $R_2 = 1$ corresponds to the companion to PSR 1957+20 filling its Roche lobe ) or a stripping rate of at least $2 \times 10^{-9} \dot{M}_{13} R_2^{-2}$ g/cm$^2$s. As a radiation length is roughly $10^2$ gm/cm$^2$, the stripping time could in principle exceed the lifetime of heavy nuclei at the surface, if there is no significant mixing of the surface layers, but it does not appear to exceed it by such a large factor that the spallation products themselves would be entirely broken up to helium and hydrogen. Moreover, the observed absorption lines, insofar as they affect the continuum, are consistent with standard solar abundances (Romani, private communication). We thus conclude that for PSR 1957+20, and similar system, the spallation of heavy elements, if it
occurs, does not defeat itself by the total destruction of either the heavy elements or the products. [Such destruction could in principle be important for some hypothetical range of parameters, (high \( f_{14.5} \), low \( \dot{M} \), requiring suppressed mass evaporation by the radiation). In this case however the destruction of primary heavy elements such as carbon would be the more conspicuous effect.]

Let us first suppose that all of the spallation products that are produced are eventually evaporated. This implies that the exposure time at the surface is set by the mass loss rate, independent of convective mixing. By the above, the fraction of carbon that is spalled to lighter nuclei can be of order \( 1.5 \times 10^{-2} f_{14.5} \left( \dot{M} / 10^{13} \text{gm/s} \right)^{-1} R_2^2 \), or unity, whichever is less. For PSR 1957+20-type parameters, this is many orders of magnitude above the cosmic values of Li, Be and B. The largest change is in the abundance of boron. The abundance levels depend on the cross-sections of the reactions that produce and destroy the respective nuclei, the photon flux and the exposure time. In the case of spallation that is just below the limit of total destruction of heavy nuclei, the ratios \( B^{10+11}/H \), \( Be^9/H \) and \( Li^7/H \) could be as high as \( 5.8 \times 10^{-4}, 5.9 \times 10^{-5}, 3.7 \times 10^{-6} \) (by number) after spallation (Boyd and Fencl 1991) compared to the cosmic ratios of \( 3.4 \times 10^{-10}, 4.5 \times 10^{-11}, 2.3 \times 10^{-9} \) respectively (Cameron 1982). We have estimated these ratios for a photon number spectrum with an index \(-2.7\), assuming that the expected spectrum of 1957+20 will be similar to that of Crab nebula (Nolan et al. 1993). These ratios change only slightly with the exact shape of the spectrum above 10 MeV. In any case, the spallation products should be above the otherwise expected levels, if the incident flux of sufficiently hard gamma radiation on the companion is a small fraction \((10^{-6} \text{ or more for 1957+20})\) of the intercepted spin down power. We suggest HST observations of the BI resonance lines near 2497Å which have been used to estimate the boron abundances in halo stars (Duncan, Lambert and Lembke 1992). Unfortunately, the reddening of 1957+20 may make observations in the UV difficult, although this does not rule out the UV observations of other sources. The Li I resonance line at 6707.8Å can be used to measure the lithium abundance (as was done for V404 Cygni, see below).

The above neglects both dilution due to turbulent convection to deeper levels, which may occur more rapidly than the stripping time, and destruction by subvection to the core. In discussing this, it is useful to note that the column density of the entire star is \( M / \pi R^2 \), where M and R are respectively the mass and radius of the star, is about \( 10^9 \) radiation lengths. If the mass evaporation is such that all of the layer down to which the mixing obtains eventually is lost, then in steady state, the mixing has no effect on the level
of spallation products at the surface. This includes the case in which the entire star is eventually evaporated. If, on the other hand, the mixing depth $\lambda_m$ is larger than the time integrated ablation depth $\lambda_a$ (which grows linearly in time), then the dilution of spallation products is simply the ratio of the two $\lambda_m/\lambda_a$. While an evaluation of the mixing depth is beyond the scope of this paper, we note that for PSR 1957+20, the layer of mass loss can be conservatively estimated from the dispersion measure of the eclipsing wind as $10^{12} g/s$ times the age $t$. For $t$ of order a spin down time, which for this particular system is roughly a Hubble time or more, the lost mass is then about $10^{-2}$ of the companion mass, so that the astrophysical uncertainty imposed by our ignorance of turbulent mixing is not all that large. Even if the system is only $\sim 3 \times 10^7$ yr old, the uncertainty in $\lambda_m/\lambda_a$ is several orders of magnitude less than the maximum light element enhancement.

The light element abundance in the gas that has been blown off from the companion, is simply the ratio of the rate of accumulation of light element nuclei to the stripping rate, apart from the dilution factor due to convection as discussed in the previous paragraph. The rate of accumulation of light elements due to spallation has been calculated by Boyd and Fencl (1991). In the limit that neither carbon nor lithium destruction is significant at the surface we can use their calculations to express the abundances of light elements (for the case of $\lambda_m > \lambda_a$) as:

$$\frac{B}{H} \sim \left( \frac{\lambda_a}{\lambda_m} \right) 8.5 \times 10^{-7} \dot{M}_{13}^{-1} R_2^2 f_{14.5},$$
$$\frac{Li}{H} \sim \left( \frac{\lambda_a}{\lambda_m} \right) 10^{-8} \dot{M}_{13}^{-1} R_2^2 f_{14.5},$$
$$\frac{Be}{H} \sim \left( \frac{\lambda_a}{\lambda_m} \right) 9 \times 10^{-13} \dot{M}_{13}^{-1} R_2^2 f_{14.5},$$

where, as argued in the preceding paragraph, the ablation depth $\lambda_a$ is a linear function of time and depends on the particular pulsar and its companion. Eqns(1) show that the resulting B abundance in the companion can be very important even in the case of deep mixing, much more than those of Li and Be. We note here that the ratio $\lambda_a/\lambda_m$ for a companion mass of 0.02 $M_\odot$ can be written as $0.1 \tau_{10} \dot{M}_{13} R_m^{-1}$, where $R_m$ is the mixing depth in units of $R_2$, and $\tau_{10}$ is the system age in $10^{10}$ yr.

We have considered the possibility that spallation products are destroyed by nuclear burning. Probably the companion star is too cool for this, if it fills its Roche lobe, in the case of 1957+20, where the companion mass is only 0.025 and the radius about 0.3 (in solar units) (Fruchter et al.1988). The central temperature is for these numbers only about
1.5 \times 10^6 \text{K}. In general, a light companion still on the main sequence could burn its spallation products; a star of 0.08 solar masses, for example, has a central temperature of $4 \times 10^6 \text{K}$, enough for lithium burning, which requires only $3 \times 10^6 \text{K}$ (Swenson, Stringfellow and Faulkner 1990), but, clearly even a modest amount of bloating would cool the companion core too much to incinerate the spallation products. The case against incineration is even stronger for Be and B, and/or lighter companions, such as in the case of 1957+20, where the central temperature may not in general be enough for incineration under any set of assumptions.

3. V404 Cygni

The lithium abundance in the secondary in the V404 Cygni system has been estimated to be of the order of $\text{Li/H} \sim 10^{-9}$, which is close to the cosmic interstellar ratio (Martin et al. 1992). This is anomalous considering the fact that the secondary is most probably a G9 dwarf star (Martin et al. 1992), and a G/K main sequence star should deplete its lithium abundance by an order of magnitude after $\sim 100 \text{ Myr}$ and by 2-3 orders of magnitude after $\sim 1 \text{ Gyr}$. In the light of the above discussion on photospallation, it seems possible that $\gamma$-radiation from the vicinity of the central object, a stellar mass black hole, can easily reimburse the lost lithium in the secondary star, as has been noted by previous authors (Martin et al. 1992, Gilmore 1992; also see discussions on photospallation and light elements in other astrophysical contexts, e.g., Boyd and Fenc1 1991, Gnedin and Ostriker 1992) (While Martin et al. (1992) proposed particle spallation in the accretion disk around the primary, spallation at the companion’s surface should work just as well). The observed abundance of lithium that is near the cosmic abundance would require a rough, coincidental balance between the production and destruction processes (at the present epoch) described in the eqns (1). However, there may be two other reasons for the preservation of Li at roughly cosmic abundances that do not require such a coincidence: Firstly, it may be that heating of the companion surface by the primary compact object merely stabilizes the outer layers to convection, so that the light elements in these layers are never subducted to the depths at which they are destroyed. Secondly, it may be that the black widow effect, if the companion is destroyed on a timescale of $\sim 10 \text{ Myr}$, selects out for observation only those systems that are too young to have suffered significant Li destruction. Theoretical analysis of the possibilities from first principles, in our view, are extremely difficult, and not in any case the primary topic of this paper. Their viability depends, as for the case of pulsar companions, on the turbulence induced by horizontal pressure gradients resulting from
uneven heating of the surface. Such turbulence, together with heat conduction, competes with outward mass flow in determining the entropy distribution in the outer layers of the heated companion, and the matter is in our view not fully resolved. But if the two “preservation” scenarios for the light elements can be observationally distinguished from the scenario of “restoration” by photospallation (the former predicting a higher ratio of Li$^7$ to the other light elements), then the results might have implications for the companions to pulsars as well.

**Conclusions**

Any model of companion irradiation by a primary pulsar in which quanta exceeding 15 Mev or so strike the companion surface predicts that the companion atmosphere be anomalously rich in Li, Be and, particularly B if the central temperature of the companion is too small to burn it. Spectroscopic observations of an ever growing number of companions to binary pulsars may prove to be a powerful diagnostic of the high energy output of the primary pulsar that is predicted theoretically.

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