Nanoscale

1. Introduction

The atomic force microscope (AFM) has found a variety of applications in molecular and cell biology.1–5 Those applications range from the generation of sub-200 nm spatial resolution maps of the stiffness of mammalian cells2–5 to the sub-5 nm mapping of the flexibility of single proteins6 or the time-resolved imaging of protein interactions and processes.7 Several AFM experiments have shown a correlation between the local stiffness of a cell with its physiological and/or pathological state.6–8,19 In general, AFM studies are strengthening our understanding of the role of mechanical properties in cell development, differentiation and physiology.

AFM methods such as force-volume,20 AFM-based micro-rheology,21 strain22 and creep relaxation23 or multifrequency24,25 have been applied to characterize the mechanical response of cells. Force-volume is by far the most common AFM-based method to generate spatially-resolved stiffness maps of cells.1,3,20,26–28 Force-volume is based on the acquisition of force–distance curves (FDC) (approach and retraction sections) on each point of the cell surface.1,20 The force–distance curve obtained by approaching the tip towards the surface (approach) might differ from the curve obtained during tip’s withdrawal (retraction). In the following a FDC always includes approach and retraction sections.

AFM measurements require to culture a cell on a solid support. Common solid supports are made of glass, plastic or very thin mica layers. Those supports are far more stiffer than a mammalian cell is. For example, the Young’s modulus of a glass cover slip is about 50 GPa while the Young’s modulus of a fibroblast cell is about 1 kPa. This is, a mammalian cell is about seven orders of magnitude softer than the solid support. The effect of this Young’s modulus mismatch on the force measured in a FDC experiment is enhanced by the finite-thickness of cell (2–15 μm).

The combination of the cell’s softness, its finite-thickness and the rigidity of solid support has given rise to the bottom-effect artefact during the acquisition of a FDC.29–32 This artefact makes cells to appear stiffer than they are. This effect, if it is not corrected, introduces significant quantitative errors in the determination of the Young’s modulus of a cell.31

Chadwick and co-workers were the first to point out that the force applied by an AFM probe on an adherent cell resting on a rigid support is influenced by the stiffness of the solid support.29,30 The first bottom-effect correction was deduced for an elastic material indented by an spherical probe.29 Bottom-effect corrections have been generalized to any axisym-
metric probes. Ros and co-workers have developed an approximate bottom-effect correction for the determination of the Young’s modulus that is valid for rigid and soft supports.

A bottom-effect correction theory gives the force as a series of terms that depend on the indentation, contact area and cell’s thickness. Bottom-effect correction models have been validated by using finite element model simulations on elastic materials. However, an earlier bottom-effect correction model developed for a conical tip acting on an elastic material fails to agree with the simulations and other models.

Living cells show a variety of viscoelastic phenomena which remain insufficiently understood. This lack of understanding has fundamental and practical implications. The accuracy of Young’s modulus measurements determined without considering viscoelastic effects is highly questionable. Finite element method simulations have shown that the Young’s modulus of a viscoelastic material deduced by using an elastic contact mechanics model could be off by a factor 5 from its expected value. The incertitudes associated with the calibration of the force constant or the determination of the contact point have been minimized by the using some standardized calibration protocols.

In a previous contribution we have proposed a bottom-effect correction model for a 3D Kelvin–Voigt (kV) viscoelastic material. The 3D-KV model was based on using the contact area determined from Hertz’s contact mechanics. It has been established that Hertz’s model overestimates the contact area for a viscoelastic material during the tip’s retraction. Therefore, Garcia and Garcia model is only valid to determine mechanical properties during the approach section of a FDC.

Raman and co-workers applied a simplified version of the correspondence principle to combine Dimitriadis et al. bottom-effect correction into Ting’s model. Their approach enables to calculate numerically the force versus the indentation for the approach and retraction sections of the FDC. The validity of Raman’s method remains to be demonstrated. Janshoff and co-workers incorporated Ting’s considerations into a model to determine viscoelastic parameters from a FDC. Janshoff’s model does not include bottom-effect corrections.

Here, we develop an analytical method to transform force–distance curves into the intrinsic viscoelastic parameters of a finite-thickness living cell deposited on a rigid support. The method is based on the application of the correspondence principle between elastic and viscoelastic deformations, Ting’s method to determine the force as a function of the deformation history and bottom-effect correction algorithms.

The method provides, for a conical probe, an analytical equation of the force as a function of the indentation. The method is valid for the approaching and retraction sections of a FDC. The theory has been deduced for several viscoelastic models, in particular, power-law rheology. The comparison between the theory and the experiments performed on fibroblast cells leads to three relevant results. First, we provide an

2. Theory of force–distance curves for finite-thickness viscoelastic materials

Fig. 1a shows a model to describe an AFM experiment performed on a cell resting on a rigid support. The cells is modeled as a finite-thickness viscoelastic layer. The goal is to obtain analytical expressions of the force as a function of the indentation I for the tip’s approach and withdrawal from the sample. This problem is divided in three steps. The determination force–distance curve exerted on a semi-infinite elastic medium, its extension to describe a semi-infinite viscoelastic material and the introduction finite-thickness effects.

The problem concerning the determination of the force exerted by a spherical probe on a semi-infinite elastic material is quite old. Sneddon generalized Hertz and Boussinesq’s considerations for any axisymmetric indenter with the following expression,

$$F = \alpha EI^\beta$$

where the coefficients $\alpha$ and $\beta$ depend on the particular geometry of the indenter; $\alpha$ might also depend on the Poisson coefficient $\nu$, however, for an incompressible material ($\nu = 0.5$),
\( \alpha \) is only a function of the tip’s shape. In what follows, a mammalian cell is considered as an incompressible material.

The expression of the force exerted by an axisymmetric probe on a finite-thickness and elastic material is given by\(^{31}\)

\[
F = \sum_{j=0}^{N} a_j E \Gamma^j. \tag{2}
\]

The coefficients \( a_j \) and \( \beta_j \) could depend on the geometry of the probe or indenter and on the finite-thickness of the material (cell). A description of the terms that appear in eqn (2) can be found in ref. 31.

### 2.1. Force–distance curves: approach

Eqn (1) and (2) describe the forces and deformations experienced by an elastic system under the application of an external load. Lee and Radok\(^{37}\) developed a method to transform the expression deduced for a semi-infinite elastic system into the force for its equivalent viscoelastic system. This method is known as the viscoelastic correspondence principle. Their methodology applied to eqn (2) gives a time-dependent force\(^{43}\)

\[
F(t) = \sum_{j=0}^{N} a_j \int_0^t \varphi_j(t-t') \frac{d}{dt} \left( \Gamma(t')^j \right) dt' \tag{3}
\]

where \( \varphi_j \) is the longitudinal relaxation function that describes the viscoelasticity of the cell; \( a_j \) and \( \beta_j \) coincide with the coefficients of the elastic equation (eqn (2)). The values of these coefficients for different geometries are deduced in ref. 43. In the ESL\(^{†}\) we provide the coefficients for a conical tip.

In what follows we consider two viscoelastic models, the Kelvin–Voigt model (KV)\(^{58}\) (Fig. 1b) and the power-law rheology model\(^{33}\) (Fig. 1c).

The relaxation function for the Kelvin–Voigt’s model is given by\(^{43,58}\)

\[
\varphi_{KV} = E + 3 \eta_G \delta(t) \tag{4}
\]

where \( E \) is the Young’s modulus, \( \eta_G \) is the shear viscosity coefficient and \( \delta(t) \) is the Dirac delta function.

The relaxation function for the power-law rheology model (PLR) is given by\(^{33}\)

\[
\varphi_{PLR} = E_0 \left( \frac{t}{t_0} \right)^{-\gamma} \tag{5}
\]

where \( E_0 \) is the apparent Young’s modulus at time \( t_0 \), \( \gamma \) is the power-law exponent and \( t_0 \) is a timescale factor which is set to 1 s.\(^{33}\) The exponent describes the viscoelastic behavior of the material. It takes values between \( \gamma = 0 \) (elastic material) and \( \gamma = 1 \) (Newtonian liquid).

In what follows we deduce the analytical solutions of eqn (3) to determine the force exerted by a conical tip (half-angle \( \theta \)) on either, KV (Fig. 1b) and PLR (Fig. 1c) finite-thickness materials. Conical tips are very common in AFM measurements performed on living cells. Therefore, this geometry does not restrict the experimental implications of the theory. We also assume that the FDCs are performed at a constant velocity \( v \) (triangular waveform) (Fig. 2).

For a KV model it has been shown that\(^{43}\)

\[
F(t) = \frac{8 \tan \theta}{3 \pi} \int_0^t \varphi_{KV}(t-t') \frac{d}{dt} \left( \Gamma(t') \right) dt' + O \left[ \frac{v^2 t^2}{h^2} \right]. \tag{6}
\]

The combination of eqn (3) and (5) leads to an expression for the force as a function of time for a PLR material

\[
F(t) = \frac{8 \tan \theta}{3 \pi} \int_0^t \varphi_{PLR}(t-t') \frac{d}{dt} \left( \Gamma(t') \right) dt' + O \left[ \frac{v^2 t^2}{h^2} \right]. \tag{7}
\]

where \( \Gamma \) is the gamma function and \( O \) is a function that includes higher order correction terms. The influence of those terms in the force is negligible.

The above expressions show that the force depends on the finite-thickness of the cell \( h \). The step-by-step process to deduce the above equations is described in the ESL\(^{†}\). We note that the above expressions are only valid to determine the force exerted by the tip during the approach, this is, for \( t < t_{max} \) where \( t_{max} \) is the time at which the maximum indentation \( I_{max} \) is reached (Fig. 2).

### 2.2. Force–distance curves: retraction

Lee and Radok’s theory\(^{37}\) is only valid to describe an experiment where the contact area increases monotonically with time, this is, for the approach section of a FDC. Ting’s method overcomes the above limitation.\(^{51,52}\)
Ting’s method assumes that for a given time \( t \) of the retraction curve there is an equivalent time \( t_1(t) \) in the approach curve that has the same contact area. The key feature of the method is that the force at time \( t \) can be obtained from eqn (3) by replacing the upper limit of the integral from \( t \) to \( t_f \). This requires to solve the integral equation which links the current time \( t \) with a previous time \( t' \) \( ^{31} \) (Fig. 3)

\[
\int_{t_f}^{t} \varphi(t') \frac{d}{dt}(I(t')) dt' = 0. \tag{8}
\]

The above equation is valid for any geometry of the tip because it does not depend on the coefficients \( \alpha_j \) and \( \beta_j \). Eqn (8) can be solved for both KV and PLR relaxation functions by assuming a constant velocity during the indentation (\( t = vt \)).

For KV we deduce

\[
t_1(t) = \frac{v(2t_{max} - t - \tau)}{\tau} \tag{9}
\]

where \( \tau = \frac{2n}{k} \) is the KV relaxation time.\(^{43}\)

For the PLR we obtain

\[
t_1(t) = t - \frac{1}{\sqrt{2}}(t - t_{max}). \tag{10}
\]

An alternative expression to eqn (10) was deduced in ref. 53. We note that eqn (9) and (10) do not depend on the tip’s geometry nor on the sample thickness.

By integrating eqn (3) with the relaxation function (eqn (4)) and \( t_1 \) given by eqn (9) we obtain the dependence of the force with the indentation while the tip is withdrawn (\( t > t_{max} \)) from a KV viscoelastic material,

\[
F(t_1) = \frac{8}{3\pi} \tan(\theta) \frac{v^2 t_1^2}{3n} + 0.721 \frac{8}{3\pi} \frac{v^2 t_1^2}{3n} + O[\eta] \tag{11}
\]

Eqn (6) (\( t < t_{max} \)) and (11) (\( t > t_{max} \)) provide the complete expression of the force (approach and retraction) as a function of the indentation for a finite-thickness KV viscoelastic material.

By integrating eqn (3) with the relaxation function (eqn (5)) and \( t_1 \) given by eqn (10) we obtain the dependence of the force with the indentation while the tip is withdrawn (\( t > t_{max} \)) from a PLR viscoelastic material,

\[
F(t_1) = \frac{8}{3\pi} \tan(\theta) \frac{v^2 t_1^2}{3n} + 0.721 \frac{8}{3\pi} \frac{v^2 t_1^2}{3n} + O[\eta] \tag{12}
\]

Eqn (7) for the approach (\( t \leq t_{max} \)) and eqn (12) for the retraction (\( t > t_{max} \)) provide the complete expression of the force as a function of the indentation for a finite-thickness PLR viscoelastic material.

3. Materials and methods

3.1. Cell culture and sample preparation

NIH 3T3 fibroblasts (Sigma-Aldrich) were cultured at 37 °C in Dulbecco’s modified Eagle’s medium–DMEM (Gibco Life Technologies, Paisley, UK). The medium has been supplemented with 2 mM L-glutamine (Sigma-Aldrich, Missouri, USA), 10% calf Serum–CS (Gibco Life Technologies) and 1% penicillin/streptomycin at controlled humidity (90%). The CO2 concentration is kept at 5%. The cell culture process was carried out in a 60 mm Petri dish (Thermo Fisher Scientific, Massachusetts, USA). The cells were extracted from the incubator after reaching an approximately 50% confluence of cells. At this point, the initial cell culture medium was exchanged by Leibovitz’s L-15 medium (Thermo Fisher Scientific) in order to maintain the pH at a value of 7.4-7.7 during the AFM experiments.

3.2. AFM-based force–distance curves

AFM measurements were performed in a commercial instrument, JPK NanoWizard 3 (JPK Instruments AG, Berlin, Germany), mounted on an Axio Observer D1 inverted microscope (Carl Zeiss, Oberkochen, Germany). The measurements

\[
\begin{align*}
&t \longrightarrow \ t_1(t) \\
&v < 0 \\
&a = a_1 \\
&F = F_1 \\
&\nu \neq \nu_1 \\
&I \neq I_1
\end{align*}
\]

Fig. 3 Scheme used to determine the force as a function of the indentation for a finite-thickness viscoelastic material. (a) In the left panel, the tip moves towards the cell (approach). In the right panel, the tip moves away from the cell (retraction). (b) Summary of Ting’s model assumptions to determine the force as a function of the indentation while the tip’s is withdrawn from the cell at a time \( t \) (retraction) based on the force measured at a previous time \( t_1(t) \) during the approach. \( F \) is the force exerted on the cell, \( a \) is the contact radius, \( \nu \) is the velocity and \( I \) is the indentation.
were performed on living cells in the aforementioned buffer. The temperature was kept constant at 37° by using a temperature controller (BioCell™, JPK Instruments AG).

We have used AC40TS cantilevers (Bruker, Camarillo, CA, USA) with a nominal spring constant of 0.09 N m⁻¹ and a conical tip shape with an estimated half-opening angle of 18°. In order to obtain reliable and quantitative data from the AFM experiments, the cantilever spring constant k was calibrated by using the thermal tuning method. This method is implemented in the software of the microscope.

The tip–sample distance was modulated by applying a triangular waveform. This implies that the velocity of the tip is constant except at the turning points. The force–distance curves were taken by using a closed-loop feedback circuit in the z-piezo axis. The piezo z-displacement was readjusted with a capacitive sensor. The FDC were obtained by applying a maximum force of 3.0 nN. The total piezo displacement was set at 5 µm while the maximum indentation was between 1 and 2 µm. The baseline region far from the cell surface was used to determine the contact point. The tip-cell contact point was determined by using the ratio of variances method. The cell’s thickness h (distance between the upper surface of the cell and the rigid substrate) was determined from an AFM topography image of the cell acquired before the FDC data.

The experimental force–distance curves were obtained on a region of 10 × 10 µm² located on the central part of the cell. The region was divided in 64 sub-regions and a FDC was measured on each sub-region. The measurements were repeated on 20 cells. Data sampling rate was set at 5 kHz for the 10 µm s⁻¹ experiments. It was increased linearly with the tip velocity to reach 150 kHz for the 300 µm s⁻¹ experiments.

4. Results and discussion

4.1. Mechanical model of a living cell

Several FDC experiments have revealed that the approach and retraction sections of force–distance curves performed on mammalian cells do not overlap.³,⁴¹,⁵⁰ The hysteresis observed in a FDC is either a consequence the existence of energy-dissipation processes inside a material³⁹,⁶⁰ or produced by the breaking of the plasma membrane. Force–distance curves acquired sequentially on a single cell are very reproducible,³,⁴¹ therefore, we conclude that the hysteresis is dominated by dissipative processes occurring inside the cell.

Fig. 4 shows a comparison among an experimental curve obtained on a fibroblast (NIH 3T3) and the corresponding curves obtained by using, respectively, the KV and PLR models. The experiment was performed on a single position of the cell above the nucleus. Fig. 4a shows the dependence of the force on time and Fig. 4b on indentation. The transformation from a force-time curve to a force–distance curve is straightforward once the parameters of the waveform that modulates the tip-cell distance are known (Fig. 4a). The experimental curve was fitted to KV (\(E = 1614\) Pa, \(\eta = 25\) Pa s) and PLR (\(E_0 = 572\) Pa, \(\gamma = 0.42\)) models. In both cases, a conical tip with a half-angle of \(\theta = 18°\) was used. The PLR model reproduces very well both sections of the FDC. The KV model gives a good fitting during the approach but it fails to reproduce the retraction section of the FDC. The force shows a jump discontinuity when the tip reaches the maximum indentation and the direction of the velocity is reversed (retraction). This result is an artefact of the KV model because in this model where the viscous force is proportional to the velocity. At \(I = I_{max}\) the velocity changes sign which causes the jump discontinuity. It indicates that the KV model is unsuitable to describe the retraction section of a FDC. In addition, the KV model cannot describe stress relaxation processes. Therefore, in the following sections, the discussion is focused on presenting the results obtained by using the PLR model.

4.2. Nanorheology of living cells from force–distance curves

Fig. 5 shows the experimental and theoretical FDCs obtained by varying the tip’s speed from 10 µm s⁻¹ to 300 µm s⁻¹. In these experiments, tip-cell contact times range from 8 ms.
(300 μm s\(^{-1}\)) to 500 ms (10 μm s\(^{-1}\)). For all the tip’s velocities, the quantitative agreement obtained between experiment and theory is excellent for both approach and retraction sections. The experimental FDCs are fitted to the constitutive equations (eqn (7) and (12)) to determine the viscoelastic parameters of NIH 3T3 fibroblast cells. Red curves (experiments) and blue curves (theory). The dashed line (black) shows the filtered waveform of the tip’s displacement during tip-cell contact (indentation). Tip of onical half-angle 18° and h = 6.2 μm.

To complete the development of a FDC-based nanorheology requires to transform the above velocities into equivalent frequencies of a sinusoidal motion. An equivalent frequency is deduced from the contact time, tip’s velocity and indentation (see ESI†). A velocity of 10 μm s\(^{-1}\) has an equivalent frequency 166 Hz while a velocity of 300 μm s\(^{-1}\) is equivalent to 5 kHz.

It is not straightforward to compare the FDC-nanorheology experiments and AFM-oscillatory microrheology data because they explore different regions of the cell, have different experimental set-ups and measure different quantities. In fact, the difficulty to compare data from different microrheology methods is rather general.\(^{35}\) Nonetheless, we note that AFM-oscillatory microrheology experiments report the existence of several viscoelastic regimes with different power-law exponents.\(^{40,61}\) In addition, experiments performed with other microrheology methods have also reported the existence of several power-law exponents.\(^{62}\)

4.3. Bottom-effect artefact: the influence of the sharpness of the tip

The influence of the rigid support stiffness on the force measured by AFM on a mammalian cell is an unavoidable consequence of the cell’s finite-thickness and softness. Furthermore, the influence of the rigid support is magnified by using tips with large contact radius.

To illustrate the bottom-effect artefact and the role of the tip’s radius (half-cone angle) we have compared the FDCs generated by the present theory and the fittings obtained by using...
Fig. 6 Dependence of the PLR parameters with the tip’s velocity. (a) Box-plot representation of $E_0$ as a function of the velocity. (b) Box-plot representation of $\gamma$ as function of the tip’s velocity. Data obtained from 20 different cells. (c) Median values of the apparent Young’s modulus. (d) Median values of the power-law exponent. Each dot is the median value of a box-plot that includes measurements on 20 different NIH 3T3 fibroblasts. The grey area marks the values of the median ± mean absolute deviation.

The above results can be explained by eqn (7) and (12). The first term in both equations is proportional to $\tan^2 \theta$ and the cell thickness $h$. The simulations show that the influence of the rigid support decreases by increasing the thickness $h$ until it reaches the true value of the material. The apparent rigid support, the one determined by using a semi-infinite theory, is reduced by the rigidity of the support. This is an artefact introduced by using a viscoelastic model that does not consider bottom-effect corrections. For the same thickness, the effect of the solid support on the apparent viscoelastic parameters decreases by decreasing the tip’s half angle. This result indicates that sharper tips should be used to measure nanomechanical properties of cells. This counter-intuitive result challenges a recommendation given to perform measurements of the elastic modulus of cells.

Similarly Fig. 7d shows that the exponent increases by increasing the thickness $h$ until it reaches the true value of the material. The apparent viscosity the material, this is the one determined by using a semi-infinite theory, is reduced by the rigidity of the support. This is an artefact introduced by using a viscoelastic model that does not consider bottom-effect corrections. For the same thickness, the effect of the solid support on the apparent viscoelastic parameters decreases by decreasing the tip’s half angle. This result indicates that sharper tips should be used to measure nanomechanical properties of cells. This counter-intuitive result challenges a recommendation given to perform measurements of the elastic modulus of cells.

The first term in both equations is proportional to $\tan^2 \theta$. This term carries exclusively information on the conical shape and on the viscoelastic properties of the material but not on its finite-thickness. The second term is proportional to the ratio between $\tan^2 \theta$ and the cell thickness $h$. Therefore, the second term carries information on the finite-thickness of the layer and of the presence of a solid support. The existence of force terms that depend on the ratio between the tangent $\theta$ (contact radius for an spherical tip) and the thickness is the key feature of analytical bottom-effect correction theories with independence of being developed for elastic or viscoelastic materials.
5. Conclusions

AFM-based force–distance curves are widely used to generate spatially-resolved maps of some elastic parameters such as the Young’s modulus or stiffness. However, in the context of cell’s nanomechanics, FDC measurements have two main limitations. First, finite element method simulations have shown that the Young’s modulus values could be off by a factor 2 to 10 from their expected values. Second, force–distance curves have been deemed unsuitable to perform nano and microrheological measurements.

The mismatch that exists between the values of the elastic parameters measured by FDCs and the expected values stems from a combination of factors. One source of error comes from the use of semi-infinite elastic contact mechanics models to describe the mechanical properties of a mammalian cell. Another limiting factor is the lack of a theory to process FDC measurements based on a realistic viscoelastic model of a cell.

We have developed an analytical method to describe the forces and deformations experienced by a cell cultured on a rigid support. The method incorporates a power-law rheology model of the cell. This viscoelastic model provides a realistic description of the mechanical response of a mammalian cell. The theory enables to determine the force applied on a cell as a function of its thickness and the indentation depth.

The theory is based on the application of the reciprocal theorem to relate pressures and deformations for different geometries, the viscoelastic correspondence principle, the deformation history of the cell and a set of boundary conditions involving a cell adhered onto a rigid support.

The analytical expressions show that the force exerted on a cell is increased by the presence of the solid support. This result is an unavoidable consequence of the boundary conditions existing in AFM experiments. Despite of this effect, the theory enables to recover the viscoelastic properties of a cell with independence of the stiffness of the rigid support.

The theoretical force–distance curves are compared with experiments performed on living fibroblasts cells. The comparison shows that for a triangular waveform, the Kelvin–Voigt model introduces a discontinuity in the force at the maximum indentation depth.
indentation which is not observed experimentally. On the other hand, there is a satisfactory quantitative agreement between the experiments and the theory based on a power-law rheology model.

The quantitative agreement is more remarkable because the power-law rheology model has just two fitting parameters, the apparent Young’s modulus and the power-law exponent. Those parameters enable to fit both sections of the FDC curves (approach and retraction). The value of the parameters depend on the effective indentation frequency. A cell is a heterogeneous and complex system with a variety of solid elements in an aqueous fluid. The above dependencies might be explained by the size of the solid elements that dominate the viscoelastic processes at a given frequency. The smaller the solid element, the shorter the relaxation time.

We show also that the cell’s mechanical parameters deduced by fitting a force–distance curve with a semi-infinite viscoelastic model are far from the expected values. The discrepancies are reduced by increasing the thickness of the material or by using sharper tips.

In summary, we have developed an analytical theory to measure the viscoelastic properties of living cells from AFM-based force–distance curves. The theory incorporates the finite-thickness of the cell, a power-law rheology model and the cell’s deformation history. Experiments performed on living fibroblast cells confirm the validity of the theory. This method will enable to overcome the semi-quantitative character of force-volume experiments on cells. In the process, it will enable to extend the use of force–distance curves to measure the nanorheological response of a cell.

Conflicts of interest

There are no conflicts of interest to declare.

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