A Fast and Efficient Conditional Learning for Tunable Trade-off Between Accuracy and Robustness

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Abstract

Existing models that achieve state-of-the-art (SOTA) performance on both clean and adversarially-perturbed images rely on convolution operations conditioned with feature-wise linear modulation (FiLM) layers. These layers require many new parameters and are hyperparameter sensitive. They significantly increase training time, memory cost, and potential latency which can prove costly for resource-limited or real-time applications. In this paper, we present a fast learnable once-for-all adversarial training (FLOAT) algorithm, which instead of the existing FiLM-based conditioning, presents a unique weight conditioned learning that requires no additional layer, thereby incurring no significant increase in parameter count, training time, or network latency compared to standard adversarial training. In particular, we add configurable scaled noise to the weight tensors that enables a trade-off between clean and adversarial performance. Extensive experiments show that FLOAT can yield SOTA performance improving both clean and perturbed image classification by up to $\sim$6% and $\sim$10%, respectively. Moreover, real hardware measurement shows that FLOAT can reduce the training time by up to 1.43× with fewer model parameters of up to 1.47× on iso-hyperparameter settings compared to the FiLM-based alternatives. Additionally, to further improve memory efficiency we introduce FLOAT sparse (FLOATS), a form of non-iterative model pruning and provide detailed empirical analysis to provide a three-way accuracy-robustness-complexity trade-off for these new class of pruned conditionally trained models.

1 Introduction

With the growing usage of DNNs in safety-critical and sensitive applications including autonomous-driving [Bojarski et al., 2016] and medical image analysis [Han et al., 2021], it has become crucial that they have high classification accuracy on both clean and adversarially-perturbed images [Wang et al., 2020]. To improve the DNN model performance against these adversarial samples, various defense mechanisms have been proposed including hiding gradients [Tramèr et al., 2017], adding noise to parameters [He et al., 2019], and detection of adversaries [Meng & Chen, 2017]. In particular, adversarial training [Madry et al., 2017; Hua et al., 2021] has proven to be a consistently effective approach in achieving state-of-the-art robustness.

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1 Adversarial images consists of imperceptible pixel perturbations from corresponding clean ones and can fool a well trained classifier models into making wrong predictions.
Figure 1: Normalized memory vs. Test accuracy for FLOAT and FLOAT with irregular sparsity (FLOATS-i) compared to the existing state-of-the-art OAT for (a) ResNet34, (b) WRN16-8, and (c) WRN40-2, respectively. CA and RA represent clean-image classification accuracy and robust accuracy (accuracy on adversarial images), respectively. For each model we normalized the memory requirement with the maximum memory needed to store corresponding model.

These defenses, however, come at various costs. Firstly, most of these methods suffer from increased training times due to the additional back-propagation overhead caused by generating perturbed images. Secondly, adversarial defenses sometimes cause a significant drop in clean-image accuracy Tsipras et al. (2018), highlighting an accuracy-robustness trade-off that has been explored both theoretically and experimentally Sun et al. (2019), Tsipras et al. (2018), Schmidt et al. (2018). Moreover, the defenses rely on several hyperparameters whose settings force the model to work at a specific point along this trade-off. This is disadvantageous in applications in which the desired trade-off depends on context Wang et al. (2020).

A naive solution to this problem is to use multiple networks trained with different priorities between clean and adversarial images. This however, comes with the heavy cost of both increased training time and inference memory. Alternatively, recent work has proposed training a once-for-all adversarial network (OAT) that supports conditional learning Wang et al. (2020), enabling the network to adjust to different input distributions. In particular, after each batch-normalization (BN) layer, they add a feature-wise linear modulation (FiLM) module Perez et al. (2018) whose weights are controlled by a parameter $\lambda$. For inference, the user sets $\lambda$ to enable an in-situ trade-off between accuracy and robustness. The disadvantage with this approach is that the added FiLM modules increase the parameter count, training time, and network latency, limiting applicability in resource-constrained, real-time applications. Moreover, our investigation shows that the CA-RA performance of OAT is heavily dependent on the choice of training hyperparameter $\lambda$. For example, the accuracy with ResNet34 on CIFAR-10 varies up to 21.97%.

Our contributions. In this paper, our contributions are two-fold. First, in view of the above concerns, we present a fast learnable once-for-all adversarial training (FLOAT). In FLOAT, we train a model using a novel mechanism wherein each weight tensor of the model is transformed by conditionally adding a noise tensor based on a binary parameter $\lambda$, yielding state-of-the-art (SOTA) test accuracy for clean and adversarial images by in-situ setting $\lambda = 0.0$ and $1.0$, respectively. For inference, we further show that model robustness can be correlated to the strength of the noise-tensor scaling factor. This motivates a simple yet effective noise re-scaling approach controlled by an user-provided floating-point parameter that can help the user to have a practical accuracy-robustness trade-off. Because FLOAT does not require additional layers to perform conditioning, it incurs no increase in latency and causes only a negligible increase in parameter count compared to the baseline models. Moreover, compared to OAT, FLOAT training is up to 1.43× faster, attributable to the fact that FLOAT does not require training with intermediate fine-grained values of $\lambda$.

Secondly, for efficient deployment of the models to resource-limited edge devices, we present FLOAT sparse (FLOATS), an extension of FLOAT, that not only provides adaptive tuning between RA and CA, but also facilitates high levels of model compression (via pruning) without incurring any additional training time. In particular, we propose and empirically evaluate the efficacy of FLOATS with both irregular and structured channel pruning, namely FLOATS-i and FLOATS-c, respectively. However, despite the potential speed-up on underlying hardware Liu et al. (2018), channel pruning often costs classification performance Kundu et al. (2021) because of its strictly constrained form of sparsity. We thus extend FLOATS to propose a globally-structured locally-irregular hybrid sparsity. In particular, we perform channel reduction through network slimming Yu et al. (2018) reducing latency and memory usage, and use irregular pruning in conjunction with this to further re-
duce memory cost. These new models not only provide compression, but enable an in-situ inference trade-off across accuracy, robustness, and complexity.

To evaluate the merits of FLOAT, we conduct extensive experiments on CIFAR-10, CIFAR-100, Tiny-ImageNet, SVHN, and STL10 with ResNet34 (on both CIFAR and Tiny-ImageNet datasets), WRN16-8, WRN40-2, respectively. As shown in Fig. 1 compared to OAT, FLOAT can provide improved accuracies of up to ∼6%, and ∼10%, on clean and perturbed images, respectively, with reduced parameter budgets of up to 1.47×. FLOATS can yield even further parameter-efficiency of up to 2.69× with similar CA-RA benefits.

2 PRELIMINARIES

2.1 NOTATION

Consider a model \( \Phi \) with \( L \) layers parameterized by \( \Theta \) that learns a function \( f_\Phi(\cdot) \). For a classification task on dataset \( X \) with distribution \( D \), the model parameters \( \Theta \) are learned by minimizing the empirical risk (ERM) as follows
\[
\mathcal{L}(f_\Phi(x, \Theta; t)),
\]
where \( t \) is the ground-truth class label, \( x \) is the vectorized input drawn from \( X \), and \( \mathcal{L} \) is the cross-entropy loss function.

2.2 ROBUST MODEL TRAINING

Several forms of adversarial training (AT) have been proposed to improve robustness [Madry et al. (2017), Samangouei et al. (2018), Buckman et al. (2018)]. They use clean as well as adversarially-perturbed images to train a model. Projected gradient descent (PGD) attack, recognized as one of the strongest \( L_\infty \) adversarial example generation algorithms [Madry et al. (2017)], is typically used to create adversarial images during training. The perturbed image for a PGD-\( k \) attack with \( k \) as the number of steps is given by
\[
\hat{x}^k = \text{Proj}_{P_t(x)}(x^{k-1} + \sigma \times \text{sign}(\nabla_x \mathcal{L}(f_\Phi(x^{k-1}, \Theta; t))))
\]
Here, the scalar \( \epsilon \) corresponds to the perturbation constraint that determines the severity of the perturbation. \( \text{Proj} \) projects the updated adversarial sample onto the projection space \( P_t(x) \), which is the \( \epsilon-L_\infty \) neighbourhood of the benign sample \( x \). \( \sigma \) is the attack step-size. For PGD-AT, the model parameters are then learned by the following ERM
\[
\min_{\Theta} \left\{ \left[ (1 - \lambda)\mathcal{L}(f_\Phi(x, \Theta; t)) + \lambda \mathcal{L}(f_\Phi(x, \Theta; t)) \right] \right\},
\]
where \( \mathcal{L}_C \) and \( \mathcal{L}_A \) correspond to the clean and adversarial image classification loss components, respectively, weighted by the scalar \( \lambda \). Hence, for a fixed \( \lambda \) and adversarial strength, the model learns a fixed tradeoff between accuracy and robustness. For example, an AT with \( \lambda \) value of 1 will allow the model to completely focus on perturbed images, resulting in a significant drop in clean-image classification accuracy. Another strategy to improve model robustness is through the addition of noise to the model weight tensors. For example, [He et al. (2019)] introduced the idea of noisy weight tensors with a learnable noise scaling factor and improved robustness against gradient-based attacks. However, this strategy also incurs a significant drop in clean image classification accuracy.

2.3 CONDITIONAL LEARNING

Conditional learning involves training a model with multiple computational paths that can be selectively enabled during inference [Wang et al. (2018)]. For example, [Teerapittayanon et al. (2016), Huang et al. (2017), Kaya et al. (2019)] enhanced a DNN model with multiple early exit branches at different architectural depths to allow early predictions of various inputs. [Yu et al. (2018)] introduced switchable BNs that enable the network to adjust the channel widths dynamically, providing an in-situ efficient trade-off between complexity and accuracy. Recently, [Bulat & Tzimiropoulos (2021)] used switchable BNs to support runtime bit-width selection of a mixed-precision network. Another conditional learning approach used feature transformation to modulate intermediate DNN features [Huang & Belongie (2017), Yang et al. (2019)].

\(^2\)Note that the generated \( \hat{x} \) are clipped to a valid range which, for our experiments, is \([0, 1] \).
Figure 2: Comparison of a conditional layer between (a) existing FiLM based approach in OAT and (b) proposed approach in FLOAT.

De Vries et al. (2017), Wang et al. (2020). In particular, Wang et al. (2020) used FiLM Perez et al. (2018) to adaptively perform a channel-wise affine transformation after each BN stage that is controlled by the hyperparameter $\lambda$ of Equation 3. Such conditional training that is able to yield models that can provide SOTA CA-RA trade-off on various $\lambda$ choices during inference are popularly known as Once-for-all adversarial training (OAT) Wang et al. (2020).

Limitations of FiLM-based model conditioning. Each FiLM module in OAT is composed of two fully-connected (FC) layers with leaky ReLU activation functions and dimensions that are integer multiples of the output feature-map channel size. Despite requiring a relatively small number of additional FLOPs, the FiLM module can significantly increase the number of model parameters and associated memory access cost Horowitz (2014). Moreover, the increased number of layers can significantly increase training time and inference latency Singh et al. (2019), thus potentially prohibiting its use in real-time applications.

Additionally, we investigated OAT’s performance on the choice of the training $\lambda$ set ($S_\lambda$), as shown in Fig. 3. Interestingly, the CA and RA can vary up to 11.03% and 21.97%, respectively. This implies that OAT’s performance may vary significantly based on both the size and specific values in $S_\lambda$. In particular, the choice of $S_\lambda$ can significantly impact the robustness at $\lambda = 0$, sometimes leading to no robustness. This implies that to obtain models that yield near optimal CA-RA trade-offs, $S_\lambda$ must be carefully chosen, implying the need for an additional compute-heavy hyperparameter search or prior user expertise.

3 PROPOSED APPROACH

3.1 FLOAT

This section details our FLOAT training strategy. We refer to the conditions for a model being trained on either clean or adversarial images as the two training boundary conditions. During training, we use a binary conditioning parameter $\lambda$ to force the model to focus on either of these two conditions, removing the need to search a more fine-grained set of $\lambda$ choices.

To formalize our approach, consider a $L$-layer DNN parameterized by $\Theta$ and let $\theta^l \in \mathbb{R}^{k^l \times k^l \times C^l_i \times C^l_o}$ represent the layer $l$ weight tensor, where $C^l_i$ and $C^l_o$ represent the number of filters and channels per filter, respectively, and $k^l$ represents the kernel height/width. We transform each parameter of $\theta^l$, by adding a noise tensor $\eta^l \in \mathbb{R}^{k^l \times k^l \times C^l_i \times C^l_o}$ scaled by a parameter $\alpha^l$ and conditioned by $\lambda$, as follows,

$$\hat{\theta}^l = \theta^l + \lambda \cdot \alpha^l \cdot \eta^l; \quad \eta^l \sim \mathcal{N}(0, (\sigma^l)^2).$$

Note that the standard deviation $\sigma^l$ of the noise matches that of its weight tensor. $\lambda = 0$ and 1 generate the original weight tensor and its noisy variant, respectively.

As illustrated in Algorithm 1, we train our models by partitioning an image batch $B$ into two equal sub-batches $B_1$ and $B_2$, one with clean ($IFM_C$) images and the other with perturbed variants ($IFM_A$) (lines 5 and 7 in Algorithm 1). We use the PGD-7 attack to generate perturbations on
the image batch $B_2$. As illustrated in Fig. 2(b), the original and noisy weight tensors are convolved only with clean and perturbed variants, respectively. Note that the noise scaling factor $\alpha^l$ (line 10) is trainable and its magnitude can be different in each layer to minimize the total training loss. The post-convolution feature maps for clean and adversarial inputs can differ significantly in their respective mean and variances [Xie et al. (2020), Xie & Yuille (2019)]. Therefore, the use of a single BN to learn both distributions may limit the model’s performance Wang et al. (2020). To solve this problem, we extend the $\lambda$-conditioning to choose between two BNs, $BN_C$ and $BN_A$, dedicated for $IFM_C$ and $IFM_A$, respectively.

Our approach differs from previous efforts in several ways. Earlier research performed noise-injection via regularization Bietti et al. (2018), Lecuyer et al. (2019) and perturbed weight tensors He et al. (2019) to boost model robustness at the cost of a significant accuracy drop on clean images. In contrast, we use noise tensors to transform a shared weight tensor and yield a model that can be configured in-situ to provide SOTA accuracy on either clean or perturbed images. Our approach is similar to $\lambda$-conditioning used by Wang et al. (2020). However, instead of transforming activations using added FiLM-based layers trained with multiple values of $\lambda$ [Wang et al. (2020)], we transform weight tensors using added noise conditioned by binary $\lambda$. Compared to Wang et al. (2020), we thus require models with significantly fewer parameters and training scenarios, yielding faster training (up to 1.43×).

**FLOAT generalization with noise re-scaling.** One limitation of the FLOAT as proposed above is that it allows the user to choose between two boundary conditions only. This limits applicability when the user is not confident about which condition to use during inference. To motivate more continuous in-situ conditioning, we analyze a ResNet20 model with noisy weight tensors trained with PGD-AT on CIFAR-10 He et al. (2019). Post-training, we re-scaled $\alpha^l$ for each layer $l$, using a new floating-point parameter $\lambda_n$ to yield $\lambda_n \cdot \alpha^l$. Interestingly, as shown in Fig. 4, as the re-scaling factor decreases, the model robustness decreases and the clean-image accuracy increases.

Based on this observation, we introduce a practical means of post-training in-situ calibration by adding a re-scaling parameter $\lambda_n$ to the inference model. This allows us to enable a practical accuracy-robustness trade-off in FLOAT during inference. We also define a threshold $\lambda_{th}$ such that for $\lambda_n > \lambda_{th}$ we select $BN_A$ to perform inference and select $BN_C$ otherwise. Wang et al. (2020) selected $BN_C$ and $BN_A$ when $\lambda = 0$ and $\lambda > 0$, respectively. We follow a similar approach by setting $\lambda_{th} = 0$.

3.2 FLOAT EXTENSION TO MODEL COMPRESSION VIA PRUNING

Pruning is a particular form of model compression that has been effective in reducing model size and compute complexity for large DNNs for resource-constrained deployment Chen et al. (2021), Kundu & Sundaresan (2021), Liu et al. (2018), He et al. (2018). Motivated by these results, we incorporate a form of pruning called sparse learning Kundu & Sundaresan (2021) into FLOAT, which we refer to FLOAT sparse-irregular (FLOATS-i). The resulting approach not only provides a CA-RA trade-off, but also meets a target global parameter density $d$. In particular, FLOATS ranks every layer based on the normalized momentum of its non-zero parameters. Based on this ranking, FLOATS dynamically allocates more weights to layer that have larger momentum and fewer weights to other layers, while maintaining the global density constraint. To be more precise, let the binary pruning mask be parameterized by the set $\Pi$ with elements $\pi^l$ representing the mask tensor for layer $l$. The fraction of 1s in $\pi^l$ is proportional to its relative layer importance evaluated through momentum. During training, the total cardinality of the masked parameters always satisfies the following constraint

$\sum_{l=1}^{L} \pi^l \leq \lambda d$.

Note that $\lambda_n$ is a continuous variable between 0 and 1 where as $\lambda$ is binary. $\lambda_n = 0$ and $\lambda_n = 1$ matches the training boundary conditions. OAT, on the other hand, uses a single variable $\lambda$ that can be any floating point value in [0, 1] during both training and inference.

Every update of the model happens sparsely, meaning only a fraction of the weights are updated, while other remains as zero.
To further ensure that the pruned models have structure and enable speed-up on a wide range of existing hardware [Liu et al. (2018)], we propose FLOATS-c that performs channel pruning. In FLOATS-c, for a layer $l$, we convert the 4D $\theta^l$ to a 2D weight matrix with $C_l^i$ rows and $(k^l)^2 C_l^j$ columns that is further partitioned in to $C_l^i$ sub-matrices of $C_l^i$ rows and $(k^l)^2$ columns. To evaluate the channel importance, we compute the Frobenius norm (F-norm) of each sub-matrix $c$ by computing $f^l_c = ||\theta^l_{\cdot c}||^2_2$. We then keep or remove a channel based on the ranking of $f^l_c$’s, enabling pruning at the channel level. As depicted in Fig. [5](a), the weight heatmaps show that for the same layer FLOATS-c can yield only 20.3% non-zero channels, while FLOATS-i retains all the channels. In fact for the same target $d$, the channel density can be 10× lower for some layers as compared to that in FLOATS-i. We note that this large scale channel reduction sometimes comes at a non-negligible accuracy drop as shown in Table [1](a).

A globally structured locally irregular pruning. To simultaneously benefit from aggressive parameter reduction via irregular pruning and width reduction via channel pruning, while maintaining high accuracy, we propose a form of hybrid compression called FLOATS slim. FLOATS slim leverages the idea of slimmable networks [Yu et al. (2018)] to train a model with channel widths that are scaled by a global channel slimming-factor (SF). On top of this, we use FLOATS-i to yield a locally irregular model with even fewer parameters for a specific SF. We perform both of these optimizations simultaneously, training with multiple SFS, including SF = 1 (Algorithm detailed in the supplementary material). Note, unlike FLOATS-c, where different layers might have different SFS, FLOATS slim yields uniform SFS for all layers. However, in FLOATS slim, a model with SF$<1.0$ is trained as a shared-weight sub-network of the model with SF$=1.0$, contrasting FLOATS-c, where only one model of a specific $d$ is trained. Fig. [5](b) depicts the weight conditioned convolution operation in FLOATS slim.

![Figure 5](image-url)

**Figure 5:** (a) Comparison of channel density (weights plotted in abs. magnitude) for FLOATS irregular and channel, for the $29^{th}$ CONV layer of WRN40-2 on STL10 while both are trained for $d = 0.3$. (b) Convolutional layer operation path for FLOATS slim. Note, the switchable BNs correspond to BNs for each SF.
Figure 6: Performance of FLOAT on (a) CIFAR-10, (b) STL10, (c) SVHN, (d) CIFAR-100, and (e) Tiny-ImageNet with various $\lambda_n$ values sampled from $S_{\lambda_n}$ for two different $\lambda_{th}$ for $BN_C$ to $BN_A$ switching. The numbers in the bracket corresponds to (CA, RA) for the boundary conditions of $\lambda = 0$ and $\lambda = 1$. $\lambda_n$ varies from largest to smallest value from top-left to bottom-right point.

4 Experimental Results and Analysis

4.1 Experimental Setup

Models and datasets. To evaluate the efficacy of the presented algorithms, we performed detailed experiments on five popular datasets, CIFAR-10, CIFAR-100 [Krizhevsky et al. (2009)], Tiny-ImageNet [Hansen (2015)] with ResNet34 [He et al. (2016)], SVHN [Netzer et al. (2011)] with WRN16-8 [Zagoruyko & Komodakis (2016)], and STL10 [Coates et al. (2011)] with WRN40-2 [Zagoruyko & Komodakis (2016)].

Hyperparameters and training settings. In order to facilitate a fair comparison, for CIFAR-10, SVHN, and STL10 we used similar hyperparameter settings as Wang et al. (2020). For CIFAR-100, we followed same hyperparameter settings as that with CIFAR-10. For Tiny-ImageNet we trained the model for 120 epochs with an initial learning rate of 0.1 and used cosine decay. For adversarial image generation during training, we used the PGD-$k$ attack with $\epsilon$ and $k$ set to 8/255 and 7, respectively. We initialized the noise scaling factor $\alpha^l$ for layer $l$ to 0.25 as described in He et al. (2019). We used the PyTorch API [Paszke et al. (2017)] to implement our models and trained them on a Nvidia GTX Titan XP GPU.

Evaluation metrics. Clean (standard) accuracy (CA): classification accuracy on the original clean test images. Robust Accuracy (RA): classification accuracy on adversarially perturbed images generated from the original test set. We use RA as the measure of robustness of a model. To directly measure the robustness vs accuracy trade-off, we evaluated the clean and robust accuracy values of models generated through FLOAT at various $\lambda$ values and compared with those yielded through OAT and PGD-AT. We used the average of the best CA and RA values over three different runs with varying random seeds, for each $\lambda$ value to report in our results.

4.2 Performance of FLOAT

Sampling $\lambda_n$. Unless stated otherwise, to evaluate the performance of FLOAT during validation we chose a set of $\lambda_n$s as $S_{\lambda_n} = \{0.0, 0.2, 0.7, 1.0\}$. Note that setting $\lambda_n$ to 0.0 or 1.0 corresponds to the values of $\lambda$ used during training. Also, we measure the accuracy of FLOAT using two different settings of $\lambda_{th}$, 0.0 (similar to OAT) and 0.5. For $\lambda_{th} = 0.5$, we update the noise scaling factor by using the following simple equation

$$
\alpha_{new}^l = \begin{cases} 
\alpha^l \cdot 2 \cdot \lambda_n; & \text{if } \lambda_n \leq 0.5 \\
\alpha^l \cdot 2 \cdot (\lambda_n - 0.5); & \text{if } 0.5 < \lambda_n \leq 1.0 
\end{cases}
$$

As depicted in Fig. 6 (a)-(e), the FLOAT models generalize well to yield a semi-continuous accuracy-robustness trade-off. Also, across all the datasets, $\lambda_{th} = 0.5$ yields a more gradual transition between the two boundary conditions. Consider the setting where $\lambda_n = 0.2$. With $\lambda_{th} = 0.5$, we observe a 4.95% improvement in CA and a reduction in RA of 12.37% on average over all five datasets when compared with $\lambda_{th} = 0.0$. The improvement in clean accuracy here can be attributed to the use of $BN_C$. However, this configuration shows a drop in CA and an improvement in RA when compared to the configuration where $\lambda_n = 0.0$. This can be attributed to the use of noisy weights (refer to Eq. 5) during inference. Thus, it can be concluded that a user who cares more...
about clean image performance than adversarial robustness should set $\lambda_{th} > 0.0$ to see a less abrupt drop in CA. Note that, because the generation of adversarial images is noisy, it is not always true that increasing $\lambda$ will always significantly improve robustness. Consequently, in some cases, we obtain improved clean image performance without a significant drop in robustness.

4.3 Comparison with OAT and PGD-AT

We trained the benchmark models following OAT and PGD-AT with $\lambda$s sampled from a set $S_\lambda = S_{\lambda_{th}}$ on three datasets, CIFAR-10, SVHN, and STL10.

Discussion on CA-RA trade-off. Fig. 7(a)-(c) show the comparison of FLOAT with OAT and PGD-AT in terms of CA-RA trade-offs. The FLOAT models show similar or superior performance at the boundary conditions as well as at intermediate sampled values of $\lambda$. In particular, compared to OAT and PGD-AT models, FLOAT models can provide an improved RA of up to 14.5% (STL10, $\lambda = 0.2$) and 34.92% (CIFAR-10, $\lambda = 0.0$), respectively. FLOAT also provides improved CA of up to 6.5% (STL10, $\lambda = 1.0$) and 6.96% (STL10, $\lambda = 1.0$), compared to OAT and PGD-AT generated models, respectively. Interestingly, for both FLOAT and OAT, in all the plots we generally see a sharp drop in robustness while moving from top-left to bottom-right. This can be attributed to the switch from $BN_A$ to $BN_C$ based on the $\lambda_{th}$, in the forward pass of the inference model.

Discussion on training time and inference latency. Due to the presence of the additional FiLM modules, OAT requires more time than standard PGD-AT to train. However, a single PGD-AT training can only provide a fixed accuracy-robustness trade-off. For example, to have trade-off with 4 different $\lambda$s PGD-AT training time increases proportionally by a factor of 4. FLOAT, on the contrary, due to absence of additional layers, trains faster than OAT. In particular, Fig. 8(a) shows the normalized per-epoch training time (averaged over 200 epochs) of OAT and PGD-AT are, respectively, up to $1.43 \times$ and $1.37 \times$ slower than FLOAT.

Network latency increases with the increase in the number of layers for both standard and mobile GPUs [Li et al. 2021, Singh et al. 2019], primarily because layers are operated on sequentially [Singh et al. 2019]. The additional FiLM modules in OAT significantly increase the layer count. For example, for each bottleneck layer in ResNet34, OAT requires two FiLM modules, yielding a total of four additional FCs per bottleneck. On the other hand, FLOAT, similar to a single PGD-AT trained model, requires no additional layers or associated latency, making it more attractive for real-time applications.

Discussion on model parameter storage cost. Unlike OAT, where the FiLM layer FCs significantly increase the parameter count, the additional BN layers and scaling factors of FLOAT represent a negligible increase in parameter count. In particular, assuming parameters are represented with 8-bits, a FLOAT ResNet34 has only 21.28 MB memory cost compared to 31.4MB for OAT. Fig. 8(b) shows that FLOAT models, similar to PGD-AT:1T, can yield up to $1.47 \times$ lower memory.

Discussion on FLOPs. Compared to the standard PGD-AT, FLOAT incurs additional compute cost of addition of noise with the weight tensor during forward pass. For example, for ResNet34 with $\sim 21.28$ M parameters, FLOAT needs similar number of additions for noisy weight transformation. However, compared to the total operations of $\sim 1.165$ GFLOPs, the transformation adds on 1.182% additional computation. Moreover, as a single addition can be up to $32 \times$ cheaper than a single FLOP [Horowitz 2014], we can gracefully ignore such transformation cost in terms of FLOPs. OAT, on the other hand, also incurs negligibly less FLOPs overhead of up to only $\sim 1.7\%$ [Wang et al. 2020].
Figure 8: Comparison of FLOAT with OAT and PGD-AT in terms of (a) normalized training time per epoch and (b) model parameter storage (neglecting the storage cost for the BN and α). (c) CONV layer compute delay on conventional ASIC (using the delay model of Eq. 7, 8, and 9) architecture [Ali et al. (2020)], evaluated on ResNet34 for CIFAR-10. Note here, PGD-AT:1T yields 1 model for a specific λ choice.

Discussion on compute delay in Von-Neumann ASIC architecture. In a conventional Von-Neumann architecture a neural network algorithm can be broken down into two dominant operations: memory read and multiply-accumulate (MAC). Based on similar assumptions, the delay model for modified CONV layer compute delay on conventional ASIC (using the delay model of Eq. 7, 8, and 9) architecture can be estimated as

\[
\tau_{\text{conv}} \approx \left[ \frac{(k^l)^2 C^i C^o}{(B/IO) N_{\text{bank}}} \right] \tau_{\text{read}} + \left[ \frac{(k^l)^2 C^i C^o}{N_{\text{Mult}}} \right] H^l W^l o_{\text{mult}}.
\]  

where \(B/IO\) is the memory input-output (IO) bandwidth and \(B_W\) is the bit-width of each weight stored in memory. \(N_{\text{bank}}\) and \(N_{\text{mult}}\) corresponds to the number of hardware memory banks and multiply units [Kang et al. (2018)]. A single memory read and multiply operation time is denoted by \(\tau_{\text{read}}\) and \(\tau_{\text{mult}},\) respectively. Their values for a 65nm CMOS process technology are 9\(\mu s\) and 4\(\mu s\), respectively [Kang et al. (2018)]. Based on similar assumptions, the delay model for modified CONV layer \(l\) for FLOAT (\(\tau_{\text{Fconv}}\)) and OAT (\(\tau_{\text{Oconv}}\)) can be estimated as

\[
\tau_{\text{Fconv}} \approx \left[ \frac{(k^l)^2 C^i C^o}{(B/IO) N_{\text{bank}}} \right] \tau_{\text{read}} + \left[ \frac{(k^l)^2 C^i C^o}{N_{\text{Mult}}} \right] (1 + H^l W^l o_{\text{mult}}) \tau_{\text{mult}},
\]

\[
\tau_{\text{Oconv}} \approx \left[ \frac{(k^l)^2 C^i C^o + 2 C^o_i}{(B/IO) N_{\text{bank}}} \right] \tau_{\text{read}} + \left[ \frac{(k^l)^2 C^i C^o}{N_{\text{Mult}}} \right] H^l W^l o_{\text{mult}} + \frac{2 C^o_i}{N_{\text{Mult}}} \tau_{\text{mult}}.
\]

Here, the first term corresponds to the read delay and remaining term(s) correspond to the delay associated with the multiplications. We ignore the energy associated with reading \(\alpha^l\) because it is negligible compared to the read energy for the other model parameters. Based on these Eqs., Fig. [8] shows the minimum, maximum, and average normalized delays with respect to the \(\tau_{\text{conv}}\). In particular, conditional CONV layer delay of FLOAT can be up to 1.66\(\times\) faster compared to that of OAT, illustrating its efficacy on conventional architecture.

4.4 Performance of FLOATS

| Algorithm | Acc. \(\% (\lambda = 0.0)\) | Acc. \(\% (\lambda = 1.0)\) | CR ↑ | CRF ↑ | Reduced storage | Potential speed-up |
|-----------|-------------------|-----------------|------|------|-----------------|-------------------|
| FLOAT    | 94.83             | 22.52           | 89.1 | 56.71 | I×              | X                 |
| FLOAT c  | 94.12             | 18.7            | 86.8 | 55.92 | 10×             | X                 |
| FLOATS c | 93.84             | 17.2            | 86.8 | 53.2  | 2.94×           | X                 |
| FLOATS slim | 94.26          | 19.1            | 88.9 | 55.44 | 4.76×           | X                 |

Table 1: Performance comparison between different compressed FLOAT variants trained on CIFAR-10 with ResNet34. ✔✔, ✔✔, and X indicate aggressive, non-aggressive, and no reduction, respectively, compared to the baseline of FLOAT.

Table [1] shows the performance of FLOATS with irregular, channel, and slimmable compression. The FLOATS slim model was trained with two representative SFs of 1.0 and 0.5 with a global target density \(d = 0.3\). We report its performance with SF= 0.5. Here, compression ratio (CR) and channel reduction factor (CRF) are computed as \(\frac{1}{\text{SF}}\) and \(\frac{1}{\% \text{of total channels present}}\), respectively. Compared to FLOAT-c, FLOATS slim requires 1.62\(\times\) less storage, results in up to 2\(\times\) speed-up, and yields
Figure 9: Performance comparison of FLOAT slim, FLOATS-i slim with OAT slim. We used ResNet34 on CIFAR-10 to evaluate the performance.

2.24% higher classification accuracy. Moreover, FLOATS slim provides us with a unique three-way trade-off between robustness, accuracy, and complexity, requiring only single training pass.

Fig. 9 illustrates the efficacy of FLOAT slim compared to OAT slim. FLOAT slim provides significantly improved performance for all tested values of $\lambda$ for both the SFs. In particular, FLOAT slim yields up to 3.6% higher accuracy. Adding sparsity, FLOATS slim yields similar accuracy improvement with up to 2.95× less parameters. Moreover, GPU hardware measurements show that our slimmable training is 1.90× faster training OAT slim.

4.5 Generalization on Various Perturbation Techniques

To demonstrate the generalization of FLOAT models on different attacks, we show their performance on images adversarially-perturbed through PGD-20 and FGSM attacks. We follow Wang et al. (2020) to generate the PGD-20 perturbations and set the number of steps to 20, keeping other hyperparameters the same as PGD-7. For FGSM, we make $\epsilon = 8/255$ following Wang et al. (2020). As shown in Fig. 10(a)-(b), under both the attacks, FLOAT can achieve in-situ accuracy-robustness trade-offs similar to that of OAT. Moreover, we have analyzed FLOAT’s robustness with an ensemble of parameter-free attacks, namely the ‘random’ variant of autoattack Croce & Hein (2020). Details of the autoattack hyperparameters are provided in the Supplementary Materials. As depicted in 10(c), compared to the PGD-AT yielded models, FLOAT consistently yields better RA with similar or improved CA.

5 Conclusions

This paper addresses the largely unexplored problem of enabling an in-situ inference trade-off between accuracy, robustness, and complexity. We propose a fast learnable once-for-all adversarial training (FLOAT) which uses model conditioning to capture the different feature-map distributions corresponding to clean and adversarial images. FLOAT transforms its weights using conditionally added scaled noise and dual batch normalization structures to distinguish between clean and adversarial images. The approach avoids increasing the layer count, unlike other state of the art alternatives, and thus does not suffer from increased network latency. We then extend FLOAT to include sparsity to further reduced complexity and latency providing an in-situ trade-off including model complexity. Extensive experiments show FLOAT’s superiority in terms of improved CA-RA performance, reduced parameter count, and faster training time.

6 Broader Impact

DNNs are well-known to be susceptible to adversarial images Szegedy et al. (2013). As their application grows in various safety-critical applications, including autonomous driving Bojarski et al. (2016), medical imaging Han et al. (2021), and household robotics Tritschler (2021), achieving model robustness without sacrificing clean image accuracy is increasingly important. This is particularly important when the image scenario is dynamic. Moreover, the increasingly portable nature of these AI-enabled devices introduces stringent storage and energy-budget limitations. To address these challenging problems, this paper presents FLOAT models that can be configured in-situ to dynamically adjust the model’s accuracy, robustness, and complexity based on the image scenario. Our approach does not require iterative (re-)training as with standard PGD-AT and trains significantly faster than SOTA alternatives. Moreover, for inference-only devices, our approach circumvents the need for re-loading alternate model parameters from the cloud to support different scenarios.

We have followed the official repo https://github.com/fra31/auto-attack to generate the attack.
avoiding the potentially significant data-transfer costs. With the increase of high-stake real-world applications that require robustness, we believe this research will form the foundation for practical AI-driven applications that can efficiently adapt to their environment. Finally, we hope this paper will motivate further work aimed at enhancing the continuity of the accuracy-robustness trade-off and developing a theoretical basis that can explain the benefits and limitations of FLOAT and conditional learning in general.

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