Near-field imaging of optical diffraction radiation generated by a 7-GeV electron beam

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(Received 4 May 2005; published 26 February 2007)

We report the first unambiguous demonstration of near-field imaging of optical diffraction radiation (ODR). The source of the ODR was an aluminum metal reflective surface with a 7-GeV electron beam passing nearby its single edge. Because of the high Lorentz factor γ involved, appreciable ODR is emitted at visible wavelengths even for impact parameters of 1 to 2 mm, so standard imaging techniques were employed. The experimental results are compared to a simple near-field model. We show that the ODR signals are sensitive to both beam size and position. Applications to multi-GeV beams in transport lines in the major synchrotron radiation facilities, x-ray free-electron lasers, energy recovering linacs, and the International Linear Collider are possible.

DOI: 10.1103/PhysRevSTAB.10.022802
PACS numbers: 41.60.Cr, 41.60.Ap

I. INTRODUCTION

There is a long-standing interest in the ability to monitor a high-energy and/or high-power electron beam’s transverse size in a nonintercepting (NI) manner [1]. Although this is routinely done in ring accelerators by imaging using the NI properties of optical and x-ray synchrotron radiation (OSR and XSR), this option is not available in linear accelerators or linear transport lines. This need has become critical in an accelerator complex such as the Advanced Photon Source (APS) where top-up operations involve injection of 7-GeV beam through a transport line into the storage ring every two minutes [2]. Beam position is routinely measured using rf beam position monitors (BPMs), but NI beam-size measurements have been a challenge. One candidate for assessing the transverse beam size is optical diffraction radiation (ODR), which is emitted when a charged-particle beam passes near the edge of a conducting surface or through an aperture in the surface. This basic radiation mechanism has been investigated for years [3–5], but to date most applications involving beam-size analysis have been based on detection of small changes in the far-field angular distribution due to beam-size effects [6–12]. These effects are often partially obscured by beam-offset and beam-divergence contributions. More recently, an unusually low-divergence beam (∼1.5 μrad) allowed ODR far-field data from a slit aperture to be analyzed for beam-size effects [13]. These data were obtained via a scanning-mirror plus detector geometry, but the scan took ten minutes. A preliminary theoretical discussion of the use of near-field ODR was given in Ref. [9].

In this paper, we report for the first time the observation of ODR by imaging with focus at the object (the metal screen) on which it is produced, i.e., the near-field source image. These near-field observations lead to an alternate paradigm for using ODR to measure relative beam size using direct near-field optical imaging to assess the beam-size dimension parallel to a metal plane’s edge. For example in this case, the relative horizontal size and position can be measured from a vertically inserted mirror edge on a single beam pulse (see the inset of Fig. 1).

We show that the ODR peak signal intensity dependence is consistent with \( \exp(-2d/\gamma A) \), where \( d \) is the distance from beam center to the screen edge, \( \gamma \) is the Lorentz factor, and \( A = \lambda/2\pi \) is the reduced observation wavelength, and that the ODR image vertical profile is qualitatively consistent with our simple analytical model. Basically, this is revealed through the 2D image/map of the induced current distribution on the screen. That is, we detect the spatial distribution of fields due to the passing charge as revealed through the photons emitted by the metal screen. Our observations are consistent with the idea that the material’s electrons are accelerated and thus radiate as the particle beam passes below the metal screen’s edge with an impact parameter \( d \) of a few mm. We show that this “image” or electromagnetic “reflection” is representative of the beam’s horizontal size and position and can therefore be used as an NI relative monitor of those parameters. In the limit as the impact parameter goes through zero and the beam is completely on the screen, the radiation reduces to the more well-known optical transition radiation (OTR), which is emitted as a charged-particle beam transits the vacuum-metal interface. The backward OTR and ODR are both proportional to the Fresnel reflection coefficients squared. By using the OTR image of the beam’s current distribution and rf BPM readings as references, we validated these NI diagnostic techniques based on ODR.

II. EXPERIMENTAL AND ANALYTICAL BACKGROUND

A. Experimental background

The ODR experiment was performed at the APS facility, which includes an injector complex with an rf thermionic
gun, an S-band linear accelerator, a particle accumulator ring (PAR) that damps the linac beam at 325 MeV, a booster synchrotron that ramps the energy from 0.325 to 7 GeV in 220 ms, and the 7-GeV storage ring. In a 24-singlets fill in the storage ring, we need to inject 2.5 to 3.0 nC per shot into the ring at two-minute intervals to maintain the stored beam current within 1% of 100 mA. The rf beam position monitors provide position readings in an NI manner, but the beam size and quality are only monitored with OSR in the injector rings. The booster synchrotron to storage ring transport line has no NI monitor of beam size at present. We can check beam size with intercepting screens, but the goal is to employ NI techniques during top-up operations. At the exit of the booster synchrotron, a dipole allows the beam to be directed to an alternate line (BTX) that ends with a beam dump. The center of this 1.94-m-long magnet is 5.84 m upstream of the diagnostics station. At the magnet exit, the vacuum chamber has a 25-mm-diameter aperture that transitions to the 50-mm-diameter beam pipe. This spur line has been used to develop our ODR diagnostics. The setup includes the upstream corrector magnets, quadrupoles, and this dipole, and then an rf BPM (single-plane striplines only), the OTR/ODR imaging station, a localized beam-loss monitor based on a Cherenkov radiation detector, the Chromox beam profiling screen, and the beam dump, as schematically shown in Fig. 1. The stripline BPM was oriented for vertical position only for the initial series of experiments in testing the ODR phenomenon, and then it was rotated 90 degrees to provide direct, complementary horizontal position readings to the ODR centroids in the subsequent set of experiments.

The ODR converter is a polished Al blade/mirror that is 1.5 mm thick, 30 mm wide, 30 mm tall, and is mounted with its surface normal at 45° to the beam direction on a stepper assembly (see the Fig. 1 inset). The assembly provides vertical positioning with an overall accuracy of ±10 μm over a span of 27.5 mm. Because of radiation safety issues, the blade was constrained to move a maximum of 7.5 mm below the centerline. The OTR and ODR signals were directed by turning mirrors and relay optics to a Sony Model XC CCD camera located 1.8 m from the source. The initial relay optics consisted of five, 50-mm diameter achromats which included one triplet [with focal lengths (f) of 150 mm, 250 mm, and 100 mm] at \( z = 340 \text{ mm} \); one singlet (f of 250 mm) at \( z = 690 \text{ mm} \); and one singlet (f = 250 mm) at \( z = 1540 \text{ mm} \). The camera sensor was at \( z = 1790 \text{ mm} \). The magnification was chosen to cover the blade edge assembly and resulted in calibration factors of 55 μm/pixel in x and 45 μm/pixel in y. These were validated by the physical size of the screen image and by stepping the blade edge known amounts. Beam charge at the station could be varied from 0.4 to 3.5 nC as extracted from the booster synchrotron at 7 GeV. The OTR signal almost saturated the camera for a beam charge of 0.4 nC.

B. Potential background light sources

In order to assess any background contributions that might contaminate the ODR signal, we calculated the OSR distribution from the main dipole that is 5.84 m upstream of the station. For the field of 0.9 T and a bending radius of 25 m, the OSR at 500 nm is a very low intensity, flat (to 20%) background on the outboard side above and below the midplane as seen in Fig. 2. The OSR polarization component parallel to the bend plane is 4 times stronger than the perpendicular component. In fact, we calculate the total OSR intensity is 100 times weaker than the predicted ODR at \( d = 1.0 \text{ mm} \) as shown in Fig. 3. A simple polarization experiment confirmed that the ODR image has a stronger vertical polarization component than horizontal, which thus precludes the dipole OSR as the source. We actually detected some OSR from other upstream sources.
such as the correctors or quadrupoles, so we adjusted the upstream vertical correctors until that background light was at or below the beam centerline. This reduced the background for ODR analysis above the beam centerline. The authors of Refs. [12,13] note a 20% background effect in their far-field data that they could not subtract.

Another possible source of light contamination of the observed ODR could be OTR from a beam halo intercepting the screen. In order to rule this out, a Cherenkov detector [14,15] operating as a beam-loss monitor was used in some of our studies to verify that the beam halo at 3.5 nC was negligible above the normal Gaussian profile intensity at impact parameters of 4 to 5 $\sigma_y$, where $\sigma_y$ is the rms vertical size. Experiments were performed both by taking five images for each blade position with an MV200 videodigitizer, which provided online analysis, and by tracking 15 to 20 measurements [EPICS process variables, or PVs, correlated using the self-describing data set (SDDS toolkit [16]) as the script commanded the blade edge position. The rf BPM readings, an upstream current monitor, the Cherenkov detector readings, and several parameters from the image processing ($x$-centroid fit, $x$-sigma fit, $y$-centroid fit, $y$-sigma fit) were tracked as well as analysis based on peak intensity to full-width half-maximum intensities and peak positions. The fits to beam profiles were Gaussian distributions since the beam had been damped by the synchrotron radiation mechanism in the booster synchrotron prior to extraction to the beam line. The Cherenkov detector readings indicated there was very little beam halo above the Gaussian profile at distances beyond 4–5 $\sigma_y$.

C. Analytical model considerations

Some further background discussion on ODR is warranted. As stated before, ODR is produced when an electron beam passes near a region where different dielectric materials are present. This is generally a vacuum-to-metal interface, and the theory [5] is usually for the far-field, Fraunhofer diffraction pattern produced by a beam passing through apertures or slits in conducting planes. In the present case, our optical system effectively integrates over angle and frequency since it is focused on the ODR source itself, i.e., the near-field image on the screen. Therefore we propose a simplified model of the near field based on the method of virtual quanta described by Jackson [17] in dealing with the photonlike fields of relativistic beams. We convolve the electron beam’s Gaussian distribution of sizes $\sigma_x$ and $\sigma_y$ with the field expected from a single electron at point $P$ in the metal plane. We wish to calculate the incoherent sum of radiation from all beam particles in a pulse emitted from a given point on the ODR radiator, i.e., at $u = P - r_o$, where $P$ is the field point with respect to the origin and $r_o$ is the position of the beam centroid with respect to the origin. The impact parameter is $b = u - r$, where $r = r(x,y)$ denotes a position in the beam measured from the beam centroid. We then can write the differential spectral intensity as

$$\frac{dI}{d\omega}(u, \omega) = \frac{1}{\pi^2} \frac{q^2}{c} \left(\frac{\omega}{v}\right)^2 \frac{\alpha^2 N}{\sqrt{2\pi\sigma_x^2\sigma_y^2}} \frac{1}{\sqrt{2\pi\sigma_x^2\sigma_y^2}}$$

$$\times \int dxdy K_1^2(ab)e^{-\left[\frac{x^2}{2\sigma_x^2}\right]}e^{-\left[\frac{y^2}{2\sigma_y^2}\right]},$$

(1)

where $\omega$ = radiation frequency, $v$ = particle velocity = $c$ = speed of light, $q$ = electron charge, $N$ is the particle number, $\alpha = 1/\gamma\lambda$, and $K_1(ab) = K_1[\alpha\sqrt{(u_x-x)^2 + (u_y-y)^2}]$ is a modified Bessel function. If we measure the unpolarized light intensity $I$, this should be proportional to $|E_x|^2 + |E_y|^2$, resulting in the $K_1^2$
dependence. The separate horizontal and vertical polarizations can be modeled in a similar manner. The incoherent photon intensity is proportional to \(N\), the number of electrons, in contrast to the case of coherent diffraction radiation in the far infrared (FIR) [18], which is enhanced by \(N^2\).

III. RESULTS AND DISCUSSIONS

A. Observations of near-field ODR characteristics

The crux of the experiment is shown in Fig. 4. First, Fig. 4(a) shows an OTR image of the 7-GeV beam. The observed beam sizes were \(\sigma_x = 1375 \pm 75 \mu m\) and \(\sigma_y = 200 \pm 25 \mu m\) for a 0.4-nC beam. In Fig. 4(b), the image ascribed to ODR for an impact parameter of \(d = 1.25\) mm and \(Q = 3.3\) nC is shown. The light emission starts 1.25 mm above the beam centerline (the dashed line in the figure). This edge distance is \(6\sigma_y\) beyond the vertical beam center, but comparable to \(\gamma\lambda\) as discussed below. At this \(d\) the ODR dominates by a factor of 60 over the calculated broad, low intensity OSR from the dipole (see Fig. 3), but ODR is about 10 times weaker than OTR in absolute terms. Further evidence for the assignment of the signal to ODR is the tracking of the signal’s vertical peak position versus the blade edge position as plotted in Fig. 5. A good linear fit was found for \(d = 0.5\) to 3 mm from the beam centerline. The rf BPM readings show the vertical beam position was the same to \(\pm 40 \mu m\) during the scan. Because of the exponential-like decay of ODR peaks vertically, the signal profiles are strongest at the smaller impact parameters in contrast to what would be expected from a broad, nearly constant OSR background. In 5-frame sum image data we actually see ODR peak signal out to the 3250- \(\mu m\) point, more than twice the nominal distance scale \(d \approx \gamma\lambda\) as seen in Fig. 6. These data are characterized by an exponential scale factor of \(\gamma\lambda/2 = 909 \mu m\) with an effective wavelength of 834 nm. This was done with beam charges of 3.3 nC, a factor of only eight more than used in the OTR imaging. In addition, the ODR \(y\) profile is shown for an impact parameter of 500 \(\mu m\). There is a truncation of this profile at around 1800 \(\mu m\) compared to the peak intensity data which we attribute to vignetting caused by a variation in the effective angular aperture across the vertical field of view. Figures 4–6, represent our original set of near-field ODR studies that did not have the benefit of laser prealignment of the optical system.

Our subsequent series of experiments were performed with an altered optical system that allowed a far-field imaging option and included laser prealignment. We also exchanged our camera for one with enhanced infrared sensitivity, the Sony XC-EI30 model. Figure 7 shows a
simple interpretation of these later experiments. We compare the rapid decrease of the Gaussian fit of the OTR vertical beam profile with \( \sigma_z = 200 \mu m \) centered at \( d = 0 \), the \( d = 1000 \) (dotted line) and 1250 \( \mu m \) (solid line) ODR image vertical profiles, and the Eq. (1) model result (dashed line) scaled to the vertical profile data.

processed video image PVs including the ODR image centroids, the Cherenkov detector readings, and the rf BPM readings. The plot in Fig. 8 shows the ODR image centroid position versus the dipole current settings. The error bars are the standard deviation based on 10-shot sampling. Position changes along the \( x \) axis of less than 50 to 100 \( \mu m \) can be sensed, even though the beam size is nominally \( \sigma_z = 1375 \mu m \). The vertical rf BPM confirmed that the vertical beam positions varied by no more than 10 \( \mu m \) during the dipole current scan. The variation of position with power supply current, or \( \mu m/\mu A \) sensitivity, agrees with that of the OTR data. Therefore, the light being imaged is produced locally by the beam in the vicinity of the screen surface and cannot be from upstream OSR effects. Subsequent experiments with the rf BPM stripline rotated 90 degrees for horizontal position tracking, gave \( \mu m/\mu A \) sensitivities within 5% of the ODR results as described in a later section.

B. Nonintercepting beam size and position monitoring applications

The potential to monitor relative beam size has been discussed in our earlier papers [19–21]. However, in this case we now have the results of vertically polarized data, and the screen, optical mirrors, lenses, and camera were prealigned with a laser positioned on the beam centerline. First, benchmark OTR image profiles were obtained by inserting the Al metal screen into the beam during a scan of the upstream AQ2 quadrupole field. This quadrupole strongly affects the horizontal beam size at our OTR/ODR station. Unfortunately, this is at a dispersive point in the lattice so we could not get emittance data cleanly from the quadrupole field scan. However, we do obtain a
test of ODR as a relative beam-size monitor. As seen in Fig. 9, the OTR-measured horizontal beam size varies from 2300 μm down to about 1300 μm. Results of the Gaussian fitting algorithms are shown since the beam shape is essentially Gaussian when extracted from the 7-GeV booster synchrotron. We also show the observed vertically polarized ODR image profiles with an impact parameter of 1.25 mm during a similar quadrupole field scan. The vertically polarized ODR horizontal image profiles track the beam-size changes as seen qualitatively by the shape of the curve with AQ2 current. This direct comparison of the OTR and ODR is seen in the Fig. 9 combined plot of their fitted rms values. The ODR profiles are about 5% to 25% larger than the corresponding OTR profiles from the largest beam size to the smallest, respectively. The ratio of ODR/OTR for the size scan is plotted in Fig. 10, which could act as a look-up table for the beam-size monitor. As can be seen, at the minimum size of 1300 μm for the OTR, the ODR fit value is only 25% larger. This is much better than our factor of 2 results with unpolarized ODR observed on the same shift for this minimum beam focus as previously reported [20]. The vertical polarization component would appear to be more reliable and direct in monitoring the actual beam size to better than 10%, once you have the ratio table or plot for these conditions.

In order to assess further the sensitivity of ODR for potential beam diagnostic applications, we have numerically evaluated Eq. (1) for fixed γλ and found qualitative support for the observed ODR Gaussian shape along the x axis, the dependence on x-beam size, and the exponential-like decay of the peak intensity along the y axis. Our calculations revealed easily detectable changes of the ODR image size by ~±15% with beam-size changes of ±20% at a central value of σx = 1300 μm as shown in Fig. 11. In this case of a highly elliptical beam, we calculated very little change in the ODR y-profile for 20% changes in the σy = 200 μm value. We also calculated that for smaller beam sizes we should use a correspondingly smaller impact parameter. For example, we found ODR image x-size changes of 25% correlate to a beam-size change from σx = 20 to 50 μm with a fixed y-impact parameter of 100 μm = 5σy, while keeping a constant σy = 20 μm. The clear effects at the half-maximum level of the ODR profile are shown in Fig. 12. This regime of beam sizes is expected in x-ray free-electron lasers (XFELs), energy recovering linacs (ERLs), APS Upgrade, CEBAF, and after the damping ring of the proposed International Linear Collider (ILC). Because of the high average power of the beams, the NI aspect is critical.

In addition, we revisited our relative beam position measurements first done with unpolarized ODR and com-
pared to the rf BPM and OTR values [20]. In this case, we again used vertically polarized ODR with an impact parameter \( \frac{d}{.0136} = 100 \, \mu\text{m} \) for the 7-GeV beam. This is relevant to XFEL beam-size monitoring and other advanced accelerators.

The plot in Fig. 13 actually compares the image centroid values from both OTR and ODR to the horizontal BPM readings. The OTR and ODR data overlap each other almost completely. This was done with the beam size \( \sigma_x = 1300 \, \mu\text{m} \) with the AQ2 quadrupole field set for the beam-size minimum. Again we believe the vertically polarized ODR component benefits the measurement sensitivity in the horizontal axis. Sensitivity at the 50- to 100-\( \mu\text{m} \) relative position level is attained. As in the case of beam-size monitoring, for the much smaller beam and impact parameter in the XFEL case, we would expect much better position sensitivity (sub-10 \( \mu\text{m} \)) subject to signal level. Correspondingly, a vertical single edge of a metal screen or aperture can be employed to obtain information on vertical position and beam size using the orthogonal or horizontal polarization component.

IV. SUMMARY

In summary, we report the first near-field experimental imaging study of ODR from a single-edge metal surface. We have demonstrated that ODR techniques are clear candidates for tracking relative changes in beam size (related to emittance and quality) and relative position in the transport line between the synchrotron and storage ring during our top-up mode. In principle, a second orthogonal blade could be used to determine beam size and position in the vertical plane (a rounder beam would help), and in general, slits or other apertures should be useful for other specific beam implementations. In applications with damped beams from a booster synchrotron, the expected Gaussian beam profile makes modeling simpler. This technique works with relatively large beam divergences, in our case 30 times that of Ref. [13]. Near-field ODR imaging should also have potential application to other third-generation rings that use top-up, as well as to the high-power systems such as the accelerator drivers for XFELs, light sources based on ERLs, and that proposed for the ILC. Effective relative size sensitivity at the 20- to 50-\( \mu\text{m} \) regime for a Gaussian beam is indicated for an impact parameter of \( 5\sigma_y = 100 \, \mu\text{m} \) according to our model, while 10-\( \mu\text{m} \) sensitivity for position should be achievable. These initial results have helped to elucidate the ODR mechanism, and it is hoped that they will also stimulate further development of nonintercepting diagnostics for present and future accelerator-based facilities.

ACKNOWLEDGMENTS

The authors acknowledge B. Yang for input on optics issues; B. Rusthoven and A. Barcikowski for the mechanical design of the stepper motor and ODR blade assembly; A. Pietryla and C. Gold for the Cherenkov detector installation; L. Emery for beam loss calculations; and J. Xu and S. Shoaf for controls for the ODR station and Cherenkov detector. We acknowledge O. Singh and W. Ruzicka for project support. One of the authors (A.H.L.) acknowledges past and recent discussions on OTR/ODR with R. Fiorito (University of Maryland) and H. Loos (SLAC), respectively. This work was supported by the U.S. Department of Energy, Office of Basic Energy Sciences, under Contract No. W-31-109-ENG-38.
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