Resolving the bow-shock nebula around the old pulsar PSR B1929+10 with multi-epoch Chandra observations

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Abstract. We have studied the nearby old pulsar PSR B1929+10 and its surrounding interstellar medium utilizing the sub-arcsecond angular resolution of the Chandra X-ray Observatory. The Chandra data are found to be fully consistent with the results obtained from deep XMM-Newton observations as far as the pulsar is concerned. We confirm the non-thermal emission nature of the pulsar’s X-radiation. In addition to the X-ray trail already seen in previous observations by the ROSAT and XMM-Newton X-ray observatories, we discovered an arc-like nebula surrounding the pulsar. We interpret the feature as a bow-shock nebula and discuss its energetics in the context of standard shock theory.

Key words. pulsars: individual PSR B1929+10—stars: neutron—X-rays: stars

1. Introduction

In 1990s, a series of powerful X-ray observatories were launched to space. Among many great results on various aspects in astrophysics, these observatories allowed a first detailed study of the X-ray emission properties of rotation-powered pulsars as a class (cf., Becker & Trümper 1997; Becker & Pavlov 2001, for a review). Most old radio pulsars, though, were still too faint for a detailed study by these satellites (cf., Sun et al. 1993; Manning & Willmore 1994; Becker & Trümper 1997; Saito 1998). Thanks to the much improved sensitivity of the XMM-Newton and Chandra observatories, a more detailed study of old pulsars became possible. Observations of PSR B0950+08; B0823+26; J2043+2740 (Becker et al. 2004; Zavlin & Pavlov 2004); B0628-28 (Becker et al. 2005); B0943+10 (Zhang, Sanwal & Pavlov 2005); B1133+16 (Kargaltsev, Pavlov & Garmire 2006); B1929+10 (Becker et al. 2006); and B2224+65 (Hui & Becker 2007a) for the first time have allowed us to study the emission properties of old pulsars as a class. Surprisingly, the X-ray emission from old pulsars seems to be dominated by non-thermal radiation processes. Thermal components (e.g., to account for the emission from hot polar caps) are not required to model the X-ray spectra of these pulsars, resulting in mostly upper limits for any thermal radiation components. Further support for an emission scenario dominated by non-thermal radiation is found by the observed temporal emission properties. Pulse pro-

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1 In standards of high energy astronomy rotation-powered pulsars are called young, middle aged, and old if their spin-down age is of the order of few times $10^3 - 10^4$ yrs, $10^4 - 10^5$ yrs, and $> 10^5$ yrs, respectively. This classification is diffuse, though, with a smooth transition in between the different groups.
Table 1. Ephemerides of PSR B1929+10

| Right Ascension (J2000) | 19h32m13.98s ± 0.002s |
|------------------------|------------------------|
| Declination (J2000)    | +10° 59′ 32.41″ ± 0.07″ |
| First date for valid parameters (MJD) | 52929 |
| Last date for valid parameters (MJD) | 53159 |
| Pulsar rotation period (s) | 0.2265182954 |
| Period derivative $P$ (10$^{-15}$ s s$^{-1}$) | 1.164739 |
| Characteristic age (10$^6$ yrs) | 3.09 |
| Surface dipole magnetic field (10$^{12}$ G) | 0.5129 |
| Dispersion Measure (pc cm$^{-3}$) | 3.178 |
| Distance (pc) | 361.10$^+$ |
| Spin-down Luminosity (10$^{33}$ ergs s$^{-1}$) | 3.89 |

*aAdopted from Becker et al. (2006)*

ments by Chatterjee et al. (2004) yielded a precise proper motion and parallax determination that translates into an accurate distance measurement of $d = 361.10$ pc and a proper motion of $V_{l} = 177.5 \pm 4$ km s$^{-1}$. The ephemerides of PSR B1929+10, which we made use of in this paper, are listed in Table 1.

The paper is organized as follows: in Sect. 2 we describe the observations and data analysis; and in Sect. 3 we summarize the results and provide a discussion in the context of a standard shock model for the nebular emission.

2. Observations and data analysis

Data analysis is restricted to the energy range 0.5–8.0 keV. All energy fluxes, however, are computed for the 0.5–10 keV band for better comparison with the results based on XMM-Newton data (Becker et al. 2006).

The object PSR B1929+10 was observed with Chandra in 2005 December 04 (Obs ID: 6657) and 2006 May 28 (Obs ID: 7230) with the Advanced CCD Imaging Spectrometer (ACIS). In both observations, PSR B1929+10 was located on the back-illuminated (BI) ACIS-S3 chip with an off-axis angle of $\sim 0.1$ arcmin. We used standard processed level-2 data. The effective exposures are $\sim 21$ ks and $\sim 25$ ks for the observations in 2005 December and 2006 May, respectively.

2.1. Spatial analysis

With the objective obtaining better statistics for the analysis, we combined both datasets to produce better images. We carefully checked and corrected the aspect offsets for each observation prior to the merging.

The combined X-ray images of the $4 \times 4$ arcmin field centered on PSR B1929+10 as well as a close-up of the central $1 \times 1$ arcmin regions are shown in Fig. 1. A compact nebula, which has an arc-like morphology somewhat resembling a bow-shock, is clearly detected around PSR B1929+10. X-ray contours were calculated at the levels of $(6 - 26) \times 10^{-6}$ counts arcsec$^{-2}$ s$^{-1}$ and overlaid on the image in Fig. 1b. Assuming this arc-like compact feature is a bow-shock pulsar wind nebula, it is interesting to estimate the stand-off angle $\theta_s$, which is a crucial parameter in discussing the shock physics (see also Sect. 3). By fitting a 2-D Gaussian model to the raw image of the field around PSR B1929+10, we obtained a full width at half maximum (FWHM) of $1.13 \pm 0.02$ arcsec (1σ error). We take this as an estimate for the lower bound of $\theta_s$.

To further examine the extent of the compact nebula, we computed the brightness profile in the energy band 0.5–8 keV from the raw image of bin size of 0.5 arcsec. We estimated the counts in sixteen consecutive boxes of dimensions $1 \times 15$ arcsec, oriented along the nebula. The vignetting corrected brightness profile and the orientation of the 16 spatial bins are shown in Fig. 2. The arc-like nebula extends up to $\sim 10$ arcsec from the pulsar before fading into the background. Because of the wings of the ACIS-S point spread function, the pulsar is expected to contribute to its surrounding nebula. To estimate this, we compared the observed data with the ACIS-S instrumental point spread function. To do so, we simulated a point source observation using MARX (ver 4.2.1). The adopted inputs were the pulsar spectrum and the same exposure, roll, and off-axis angle as in the actual data. We then computed the brightness profile of the simulated data in the same way as aforementioned. The estimated point source profile is shown in Fig. 2 as a dotted line. The brightness profile of the arc-like nebula computed from the actual observation is significantly different from the expected distribution of a point source. On the other hand, there is no significant extended emission detected ahead of PSR B1929+10.

![Fig. 2. Vignetting corrected brightness profile of the field around PSR B1929+10. The energy range is 0.5–8 keV. The profile expected for a point source is indicated by a dotted line. The average background level and its 1σ deviation are indicated by horizontal lines, which were calculated by sampling the source-free regions around the pulsar within a $1 \times 1$ arcmin field-of-view. The inset shows the sixteen bins used in computing the profile. Each bin is 1″ × 15″.](image-url)
trail region near the pulsar, as detected by XMM-Newton, is \( \sim 60\% \). The unabsorbed X-ray flux of a 1 arcmin circular MOS1 image with the contours calculated from XMM-Newton PSF. The smoothed image is displayed in Fig. 3. Comparing the image with the contours calculated from XMM-Newton MOS1/2 data, a faint trail like feature is noticed. However, the background contribution of this feature is estimated to be \( \sim 60\% \). The unabsorbed X-ray flux of a 1 arcmin circular trail region near the pulsar, as detected by XMM-Newton, is \( f_X = 5.3 \times 10^{-14} \text{erg/s/cm}^2 \) within the 0.5–10 keV band (Becker et al. 2006). The low significance of the trail in the two Chandra observations, thus, is in agreement with Chandra’s lower sensitivity. We, therefore, will not further consider the X-ray trail emission in this paper, and alert the interested reader to the XMM-Newton results reported by Becker et al. (2006), for a detailed discussion of its emission properties.

2.2. Spectral analysis

Although the spectrum from PSR B1929+10 has already been tightly constrained by the XMM-Newton data (Becker et al. 2006) it is important for us to re-examine its spectral properties with Chandra since it resolves the pulsar emission from the compact surrounding nebular component better.

We extracted the pulsar spectrum in both data sets from a circle of 2 arcsec radius (encircled energy \( \sim 95\% \)), centered on the pulsar, and fitted them simultaneously. The background spectrum was extracted from a source-free region within a 10 arcsec radius centered at R.A. = 19\(^{h}\)32\(^{m}\)14.107\(^{s}\), Dec. = 10\(^{\circ}\)59\(^{\prime}\)51.57\(^{\prime\prime}\) (J2000). After background subtraction, 593 \( \pm \) 24 and 682 \( \pm \) 26 net counts were available for the spectral analysis. These values imply the net counting rates of \( (2.84 \pm 0.11) \times 10^{-2} \text{cts} \) and \( (2.77 \pm 0.11) \times 10^{-2} \text{cts} \) for the observations in 2005 December and 2006 May, respectively.

We computed the response files with the tools MKRMF and MKARF in CIAO 3.4. Utilizing the most updated calibration data, CALDB 3.4.1, the generated response files corrected the degradation of the quantum efficiency in the ACIS CCD, accordingly. Each spectrum was dynamically binned so as to have at least 30 counts per bin. To better constrain the spectral properties, we fitted simultaneously the spectra obtained from both observations. We performed all the spectral fittings in 0.5–8 keV with XSPEC 11.3.2. The parameters of all fitted model spectra are summarized in Table 2. All the quoted errors are \( 1 - \sigma \), and were computed for 1 parameter of interest.

Among the single component models tested, we found that

\[
\begin{align*}
\text{a.} && \chi^2 &= 0.89 \text{ for 36 D.O.F.}, \\
\text{b.} && \chi^2 &= 2.40 \pm 0.34 \times 10^{21} \\
\text{c.} && \chi^2 &= 2.91 \pm 0.13 \times 10^{21} \\
\end{align*}
\]

We found that a power-law model fits the data best (\( \chi^2 = 0.89 \) for 36 D.O.F.). This model yields a column density of \( N_H = 2.40 \pm 0.34 \times 10^{21} \text{cm}^{-2} \), a photon index of \( \Gamma = 2.91 \pm 0.13 \), and a normalization at 1 keV of \( 8.12 \pm 0.96 \times 10^{-5} \) photons keV\(^{-1}\) cm\(^{-2}\) s\(^{-1}\). These best-fit values are fully consistent with those obtained by XMM-Newton for power-law fits (see Table 3 in Becker et al. 2006). The best-fit power-law spectrum and residuals are shown in Fig. 2.

\[
\begin{align*}
\text{a.} && \chi^2 &= 0.89 \text{ for 36 D.O.F.}, \\
\text{b.} && \chi^2 &= 2.40 \pm 0.34 \times 10^{21} \\
\text{c.} && \chi^2 &= 2.91 \pm 0.13 \times 10^{21} \\
\end{align*}
\]
counts arcsec

patchy in the region around PSR B1929 by Slowikowska et al. 2005, the interstellar medium is very
the pulsar (Slowikowska et al. 2005). However, as discussed
(XMM) measurements of the stars in the neighborhood of
7 \times 10^{30} \text{ ergs s}^{-1} \text{ cm}^{-2}$ within 0.5 – 10 keV. At
implying a luminosity of $L_X = 3.9 \times 10^{30}$ ergs s$^{-1}$.

As for the XMM-Newton data it is obvious that the single
power-law model already describes the observed pulsar spectrum
very well. Hence, the justification of including an additional thermal component is absent. In the Chandra data, we
found that fitting with a power-law plus blackbody model does
not yield a reasonable solution if we allow the blackbody radius
and the temperature to be free parameters. It resulted in a black-
body radius of $R_{bb} = 25.81^{+18.34}_{-25.81}$ m. This is much smaller than
the canonical size of a polar cap, $r_{pc} = R(2 \pi R/cP)^{1/2} \sim 300$ m,
which suggests the contribution from the additional blackbody component is insignificant. We quantified the statistical signifi-
cance for adding this extra component to the power-law model
with the $F$-test which suggests that inclusion of this thermal components is only required at a confidence level of 26%.

We have also examined the possible contributions from a polar cap and the neutron star surface by fixing the blackbody radii at $R = 300$ m and $R = 10$ km, respectively. These fits yield temperatures of $T \sim 8.7 \times 10^5$ K and $T \sim 5.6 \times 10^5$ K.
The $F$-test suggests that adding these thermal components to the power-law model is only significant at a confidence level
$\leq 62\%$. Due to the better photon-statistics this number was
even smaller in the XMM-Newton data (Becker et al. 2006). This low significance is also reflected by the relative contribu-
tion of the thermal component in the total energy flux observed
by Chandra. We estimated the $1\sigma$ upper limits for the polar cap
temperature and its flux contribution by adding a blackbody component to the power-law model. Fixing the blackbody ra-
dius at a polar cap size of $R = 300$ m, a $1\sigma$ upper limit of $T < 1.2 \times 10^6$ K was computed by assuming contribution from
one polar cap only. This implies that the $1\sigma$ limit contribution
from the polar cap in the total energy flux is $\sim 12\%$.

For the spectral model consisting of two blackbody components, we found that the best-fit model parameters also
agree well with those inferred from the XMM-Newton spec-
tra (Becker et al. 2006). Despite the acceptable value of the
goodness-of-fit, the inferred blackbody radii are too small to be considered as a reasonable description. Moreover, the pul-
sar spectrum obtained by XMM-Newton and fitted together
with the spectrum obtained by the ROSAT PSPC have already
shown that this model cannot describe the data beyond $\sim 5$ keV
(see Becker et al. 2006).

Since the arc-like nebula is resolved by Chandra for the first time, it is instructive to examine its energy spectrum, de-

Fig. 4. Energy spectra of PSR B1929+10 as observed with the Chandra ACIS-S3 detector on 04 Dec 2005 and 28 May 2006
and simultaneously fitted to an absorbed power-law model (upper panel) and contribution to the $\chi^2$ fit statistic (lower panel).

![Chandra ACIS-S3](image)

Fig. 3. The 5 × 5 arcmin region around PSR B1929+10 in the energy band of 0.5 – 8 keV. The image is created by merging both Chandra observations. It has a binning factor of 2 arcsec
and is adaptively smoothed with a kernel of $\sigma < 6$ arcsec. Top is north and left is east. The contours from the XMM-Newton’s MOS1/2 0.2–10 keV band image at the levels of 0.09 and 0.44
counts arcsec$^{-2}$ are overlaid. The proper motion corrected pulsar position is indicated by the white cross. The proper motion
direction of the pulsar is indicated by the arrow in the image.
The radius of the blackbody emitting area is calculated for an assumed pulsar distance of 361 pc.

The normalization constant for the power-law model.

Parameter of interest for the power-law model fitted to the spectrum of PSR B1929+10.

\[ \chi^2_{\nu} = \frac{1}{2} \sum_{i=1}^{n} \left( \frac{y_i - \hat{y}_i}{\sigma_i} \right)^2 \]

\[ \frac{\Gamma}{kT} \]

\[ N_H \]

\[ \text{Normalization at 1 keV} \]

\[ \text{Radius} \]

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**Table 2.** Spectral parameters inferred from fitting the Chandra ACIS-S data obtained from PSR B1929+10 and its associated extended feature.

| Model       | \( \chi^2_{\nu} \) | D.O.F. | \( N_H \) | \( \frac{\Gamma}{kT} \) | Normalization at 1 keV | Radius |
|-------------|---------------------|--------|------------|-----------------------------|------------------------|--------|
| **PSR B1929+10** |                     |        |            |                             |                        |        |
| PL          | 0.89                | 36     | 2.40\(^{+0.36}_{-0.34}\) | 2.91\(^{+0.16}_{-0.13}\) | 8.12\(^{+1.04}_{-0.90}\) \times 10^{-5} | -      |
| BB          | 2.00                | 36     | < 0.04     | 0.36\(^{+0.01}_{-0.01}\) | -                      | 29\(^{+2}_{-2}\) |
| PL+BB       | 0.93                | 34     | 1.40\(^{+1.09}_{-1.40}\) | 2.48\(^{+0.52}_{-0.29}\) | 6.60\(^{+0.29}_{-0.29}\) \times 10^{-5} | 25.81\(^{+18.34}_{-25.81}\) |
| PL+BB       | 0.92                | 35     | 2.44\(^{+0.60}_{-0.39}\) | 2.91\(^{+0.16}_{-0.13}\) | 8.17\(^{+1.09}_{-0.94}\) \times 10^{-5} | 300    |
| PL+BB       | 0.90                | 35     | 2.72\(^{+1.06}_{-0.55}\) | 2.97\(^{+0.27}_{-0.17}\) | 8.67\(^{+2.25}_{-1.22}\) \times 10^{-5} | 10000  |
| BB+BB       | 0.91                | 34     | < 0.70     | 0.71\(^{+0.21}_{-0.13}\) | 2.97\(^{+0.16}_{-0.13}\) | -      | 5.3\(^{+3.43}_{-2.30}\) \times 10^{-4} | 42.32\(^{+22.74}_{-4.47}\) |
| **Arc-like feature** | | | | | | |
| PL          | 0.88                | 6      | 2.40       | 2.00\(^{+0.32}_{-0.30}\) | 3.63\(^{+0.78}_{-0.74}\) \times 10^{-6} | -      |

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\( a \) PL = power-law; BB = blackbody

\( b \) The entry in this column depends on the model in interest. It is the temperature \( kT \) in keV or the photon index \( \Gamma \)

\( c \) The normalization constant for the power-law model.

\( d \) The radius of the blackbody emitting area is calculated for an assumed pulsar distance of 361 pc.

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**Fig. 5.** 1\( \sigma \), 2\( \sigma \) and 3\( \sigma \) confidence contours calculated for 1 parameter of interest for the power-law model fitted to the spectrum of PSR B1929+10.

**Fig. 6.** 1\( \times \) 1 arcmin raw image (0.5 – 8 keV) centered on PSR B1929+10. Data from both Chandra observations were used. The extraction regions used for the spectral analysis of the arc-like feature are illustrated.

The background spectra were extracted from each dataset within a nearby source-free region of a 10 arcsec radius, despite the poor photon statistics. We extracted the nebular spectra from the regions in accordance with its observed morphology. For the sake of consistency, we adopted the same extraction regions in both datasets, which are illustrated in Fig. 6. It consists of an annular region centered on the pulsar position with inner and outer radii of 2 arcsec and 5 arcsec, a circular region with a radius of 2.2 arcsec, as well as a ellipse of 4 arcsec\( \times \)8 arcsec.
centered at RA.=19h32m15.470s and Dec.:+10°59'29.01" (J2000). After background subtraction, there were 29 ± 5 and 41 ± 7 net counts extracted from the arc-like feature, implying the net counting rates of (1.29 ± 0.26) × 10⁻³ counts/s and (1.65 ± 0.28) × 10⁻³ counts/s for the observations in 2005 December and 2006 May, respectively. Within the 1σ errors of these count rates, no variability is apparent on the basis of these two observations. The response files were computed in the same manner as those for the pulsar spectra. Each spectrum was dynamically binned so as to have at least 10 counts per bin. In order to obtain a better statistic, we analyzed both spectra simultaneously.

We hypothesized that the nebular emission originates from the interaction of the pulsar wind and the ISM. Synchrotron radiation from the ultra-relativistic electrons is generally believed to be the emission mechanism of the pulsar wind nebula, which is characterized by a power-law spectrum. We tested this hypothesis by fitting an absorbed power-law model to the nebular spectra. We fixed the column density at the value $N_H = 2.4 × 10^{21}$ cm⁻² inferred from fitting the pulsar spectrum. The power-law model describes the observed spectrum reasonably well ($\chi^2 = 0.88$ for 6 D.O.F.). The best-fit power-law spectrum and residuals are shown in Fig. 7. This model yields a photon index of $\Gamma = 2.00^{+0.32}_{-0.30}$ and a normalization at 1 keV of $3.63^{+0.78}_{-0.74} × 10^{-6}$ photons keV⁻¹ cm⁻² s⁻¹. The unabsorbed flux deduced for the best-fitted model parameters are $f_X = 1.7 × 10^{-14}$ erg s⁻¹ cm⁻² in the energy range of 0.5 - 10 keV. The pulsar distance of 361 pc implies a luminosity of $L_X = 2.7 × 10^{29}$ erg s⁻¹.

We have checked the robustness of all the spectral parameters quoted here by incorporating background spectra extracted from different source-free regions. We found that within the 1σ errors the spectral parameters inferred from independent fittings are all consistent with each other.

### Table 3. Unabsorbed fluxes, luminosities, and the conversion efficiencies of PSR B1929+10 and the nebular components in 0.5 – 10 keV

| Component       | $f_X$ (erg s⁻¹ cm⁻²) | $L_X$ (ergs s⁻¹) | $L_X/E$ |
|-----------------|----------------------|------------------|---------|
| PSR B1929+10    | $2.5 × 10^{-13}$     | $3.9 × 10^{30}$  | $1.0 × 10^{-3}$ |
| Trail-like feature $^b$ | $5.3 × 10^{-14}$ | $8.3 × 10^{29}$  | $2.1 × 10^{-4}$ |
| Arc-like feature | $1.7 × 10^{-14}$     | $2.7 × 10^{29}$  | $6.9 × 10^{-5}$ |

$^a$ Luminosities are calculated at the assumed pulsar distance of 361 pc

$^b$ Adopted from Becker et al. (2006)

### 3. Discussion

Complementing the XMM-Newton observation, we have studied PSR B1929+10 and its surrounding medium with Chandra, which provides data with sub-arcsecond resolution. So far, three distinct components have been resolved, namely the pulsar itself, the X-ray trail opposite to the pulsar’s proper motion direction as well as the arc-like nebula surrounding the pulsar. The flux contributions from these components and the corresponding X-ray conversion efficiencies are summarized in Table 3.

The morphology of the arc-like nebula and the orientation with respect to the pulsar’s proper motion direction suggest a bow-shock nature. This is the first well-defined bow-shock morphology observed from an old pulsar.

A bow-shock nebula as observed in PSR B1929+10 can be produced by a pulsar in supersonic motion. In this case, the termination shock radius $R_s$ is determined by the balance of the ram pressure between the relativistic pulsar wind particles and the ISM at the head of the shock (cf. Hui & Becker 2007b):

$$R_s \approx \left( E/2\pi \rho_{ISM} v_p^2 c^2 \right)^{1/2} \sim 3 \times 10^{16} E_{34}^{1/2} n^{-1/2} v_{p,100}^{-1} \text{ cm}$$

where $v_{p,100}$ is the velocity of the pulsar in units of 100 km s⁻¹, $E_{34}$ is the spin-down luminosity of the pulsar in units of 10³⁴ erg s⁻¹; and $n$ is the number density of the ISM in units of cm⁻³. A density of 1 cm⁻³ implies a shock radius of $R_s \sim 10^{16}$ cm. The stand-off angle $\theta_s$ between the pulsar and edge of the shock in the forward direction is related to $R_s$ by $\theta_s = R_s \cos i/D$, where $D$ is the distance to the pulsar and $i$ is the inclination angle between the proper motion and the plane of the sky. Taking the FWHM resulted from Gaussian fitting to the radial profile (i.e., 1.13 arcsec) as the lower limit of $\theta_s$, $i$ is then constrained to be $\leq 50°$.

At a distance of 361 pc, the proper motion velocity and the size of the arc-like nebula imply the pulsar took $\sim 150$ years to pass through the sky region of the nebula. We estimated the magnetic field in this shocked region by equating the passage time to the synchrotron cooling timescale $\tau_{syn} = 6 \pi m_e c / \gamma \sigma_T B^2 \sim 10^5 (h v / k e V)^{-0.5} B_{\mu G}^{-3/2}$ yr, where $\gamma$ is the Lorentz factor of the wind, taken to be $10^8$ (cf., Cheng et al. 2004), $\sigma_T$ is the Thompson cross section, and $B_{\mu G}$ is the magnetic field strength in micro-Gauss.

![Fig. 7. Energy spectra of the arc-like structure associated with PSR B1929+10 as observed by the Chandra ACIS-S3 detector on 04 Dec 2005 and 28 May 2006, and simultaneously fitted to an absorbed power-law model (upper panel) and contribution to the $\chi^2$ fit statistic (lower panel).](image-url)
magnetic field in the shocked region in units of micro gauss. This implies a magnetic field of \( \sim 75 \mu G \) for the region near to the pulsar. For comparison, the typical field strength in the ISM is \( \sim 2 - 6 \mu G \) (cf., Beck et al. 2003, and references therein). If the magnetic field in the neighborhood of PSR B1929+10 is comparable with this estimate, the inferred compression factor is \( \sim 13 - 38 \) in the bow-shock region, which is rather high in comparison with other pulsar wind nebulae (e.g., Hui & Becker 2006, 2007b). Polarization measurements of the sky region around PSR B1929+10 in the radio band can help to better constrain the magnetic field of this system and hence the compression factor.

In the context of the standard shock theory (Chevalier 2000), the X-ray luminosity and spectral index depend on the inequality between the characteristic observed frequency \( v_{\text{obs}} \) and the electron synchrotron cooling frequency:

\[
v_e = 18\pi^2me^2/\sigma_T^2\gamma^2B^2 \quad (\text{cf., Chevalier 2000 and references therein}),
\]

which is estimated to be \( v_e = 1.8 \times 10^{17} \) Hz. Since, in general \( v_{\text{obs}} > v_e \), this suggests the X-ray emission is in a fast cooling regime.

We further probed the energy distribution of the synchrotron radiating electrons in the shock. The emitting electrons are distributed as \( N(\gamma) \propto \gamma^{-\alpha} \). In a fast cooling regime, the theoretical luminosity per unit frequency is given by (cf., Cheng et al. 2004):

\[
L_{\nu,p}^{\text{th}} = \frac{1}{2} \left( \frac{p - 2}{p - 1} \right)^{p - 1} \left( \frac{6e^2}{4\pi^2mc^2} \right)^{p - 1} \epsilon_{\nu}^{-p - 1} \epsilon_{\nu}^{-p - 2} R_e \frac{E_{\text{th}}}{E_{\nu}} \gamma^{-\alpha}. (2)
\]

Assuming the energy equipartition between the electron and proton, we took the fractional energy density of electrons \( \epsilon_e \) to be \( \sim 0.5 \) and the fractional energy density of the magnetic field \( \epsilon_B \) to be \( \sim 0.01 \). We then integrated Eq. 2 over the frequency:

\[
L_{\nu,p}^{\text{th}} = \int L_{\nu,p}^{\text{th}} d\nu,
\]

with \( \nu_{\text{min}} = 0.5 \) keV and \( \nu_{\text{max}} = 10 \) keV.

Equating \( L_{\nu,p}^{\text{th}} \) and the observed luminosity of the arc-like nebula results in an index of \( p = 2.35 \) for the electron spectrum. This estimate lies within the acceptable range of the index \( p \) as suggested in a standard shock model, i.e., \( p \sim 2 - 3 \) (cf., Cheng et al. 2004 and references therein). For a fast cooling scenario, the photon index is related to \( p \) as \( \Gamma_{\nu} = (p + 2)/2 \). The value \( p = 2.35 \) implies a photon index of \( \Gamma_{\nu} = 2.18 \). This theoretical value lies within a \( 1\sigma \) uncertainty of the observed value.

The arc-shaped morphology of the nebula observed in PSR B1929+10 is similar to that of Geminga (Caraveo et al. 2003). However, there is a main difference between these two cases. While the arc-like nebula of Geminga is rather symmetric with respect to the direction of proper motion, asymmetry is indicated in the case of PSR B1929+10 (see Fig. 1b). Its asymmetric shape might be a result of the anisotropic pulsar wind and/or inhomogeneities in the surrounding ISM (see Hui & Becker 2006).

For the pulsar PSR B1929+10, we found that the spectral properties inferred from our analysis are in good agreement with the results obtained by XMM-Newton, which did not allow the pulsar emission to be separated from the compact nebular component. The consistency is expected even in the presence of the diffuse compact nebulae as it contributes only \( \sim 7\% \) to the observed energy flux (see Table 3). Thus, the non-thermal emission scenario of PSR B1929+10 is confirmed. Hui & Becker (2007a) had argued that it is possible to sustain particle acceleration regions in PSR B1929+10’s outer-magnetosphere (so-called outer-gap) if the inclination of the magnetic axis with respect to the rotational axis is taken into account. This inference is supported by the ability of the outer-gap model in reproducing the observed X-ray pulse profile and its phase shift relative to the radio pulse (see Fig. 16 Becker et al. 2006). However, this model has difficulty in explaining the observed spectral properties of PSR B1929+10.

In the outer-gap model, the non-thermal X-rays result from the back-flowing charge particles from the outer gap (Cheng & Zhang 1999). When the primary electrons/positrons leave the outer-gap, they will emit curvature photons that are subsequently converted into secondary pairs in the presence of the strong magnetic field. Synchrotron photons will then be emitted by these secondary electrons/positrons. If these photons are energetic enough, they will further be converted into pairs that again lose their energy via synchrotron radiation. Therefore, an electromagnetic cascade is developed. Based on this model, Cheng & Zhang (1999) argued that the X-ray photon index resulting from such cascades should be \( \leq 2 \). This is obviously not in agreement with the observed photon index for PSR B1929+10, which is as steep as \( 2.91_{-0.13}^{+0.16} \). Observations of five other old pulsars: B1133+16 (Kargaltsev, Pavlov & Garmire 2006); B0943+10 (Zhang, Sanwal & Pavlov 2005); B0628-28 (Becker et al. 2005); B0823+26 (Becker et al. 2004); and J2043+2740 (Becker et al. 2004), also found the photon indices steeper than 2. This gives the outer-gap emission model a challenge. Re-examination of the model is thus required.

After this work was submitted to A&A for publication, we became aware that a paper on the similar subject as presented here was submitted to ApJ by Misanovic, Pavlov, & Garmire (2007). The results reported by these authors agree well with the results presented here. Misanovic et al., though, report to have detected a thermal component in the spectrum of PSR B1929+10. While their parameters inferred from the single power-law fittings are consistent with ours, they suggested that a model of power-law plus blackbody model provides a statistically better description. This obviously contradicts with the conclusion presented here and in Becker et al. (2006). From a closer inspection of their spectral fits we conclude that their apparent detection is probably biased by a too small signal-to-noise ratio per spectral bin. While we binned the Chandra spectrum so as to have at least 30 counts per bin Misanovic et al. (2007) grouped the data so as to have only about 15 counts per spectral bin. For the spectral fitting of XMM-Newton data, the parameters obtained by Misanovic et al. (2007) are for 190 degree of freedom whereas Becker et al. (2006) had only 121 degrees of freedom for their analysis. Becker et al. (2006) thus used a much higher photon statistics per spectral bin. The higher signal-to-noise ratio per spectral bin yielded a more stringent discrimination among competing spectral models. For this reason, the spectral results presented here as well as in Becker et al. (2006) provide more stringent constraints on the pulsar’s X-ray emission properties than those in Misanovic et al. (2007).
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