Measurement of the Neutrino Asymmetry Parameter $B$ in Neutron Decay

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A new measurement of the neutrino asymmetry parameter $B$ in neutron decay, the angular correlation between neutron spin and anti-neutrino momentum, is presented. The result, $B = 0.980^{+50}_{-120}$, confirms earlier measurements but features considerably smaller corrections. It agrees with the Standard Model expectation and permits updated tests on "new physics" in neutron decay.

Assuming only Lorentz invariance, the decay probability for polarized neutrons is given by

$$
\frac{d\omega}{d\Omega_{n}} = K \frac{dE}{d\Omega_{e}} \frac{d\nu}{d\Omega_{\nu}} \left( 1 + a \frac{p_{e}p_{\nu}}{EE_{\nu}} + b \frac{m_{e}}{E} \right) + (s_{n}) \left[ A \frac{p_{e}}{E} + B \frac{p_{\nu}}{E_{\nu}} + D \frac{p_{e} \times p_{\nu}}{EE_{\nu}} \right].
$$

$p_{e}, p_{\nu}, E, E_{\nu}$ are momentum and energy of electron and anti-neutrino (in the following called neutrino), respectively, $m_{e}$ is the electron mass, $(s_{n})$ is the neutron spin polarization, and the $\Omega_{i}$ denote solid angles. The parameters $a, A, B,$ and $D$ are angular correlation coefficients: $a$ is the correlation between the momenta of electron and neutrino. The parity violating parameters $A$ and $B$ for electron and neutrino asymmetry correlate the neutron spin with the momentum of electron and neutrino, respectively. The subject of this paper is a precise measurement of $B$.

The factor $K$ and the correlation coefficients are related to the couplings of the theory. Within the Standard Model of Particle Physics (SM), $b$ vanishes and $D$ is much smaller than the present experimental limit. $K = G_{F}^{2} |V_{ud}|^{2} F(E)(g_{V} + 3g_{A}^{2})$, with Fermi-constant $G_{F}$, quark mixing matrix element $V_{ud}$, phasespace factor $F(E)$, and vector and axial-vector coupling constants $g_{V}$ and $g_{A}$. All correlation coefficients are functions of $\lambda = g_{V}/g_{A}$, where $g_{A}$ and $g_{V}$ are assumed to be real, e.g.: $A = -2 \frac{\lambda^{2} + \lambda}{1 + 3\lambda^{2}}$ and $\delta = 2 \frac{\lambda^{2} - \lambda}{1 + 3\lambda^{2}}$.

Small higher order corrections must be considered additionally. The structure of the weak interaction ($V - A$ in the SM) is not predicted by theory but has to be determined experimentally. Due to its sensitivity to the neutrino helicity the neutrino asymmetry parameter $B$ is an important input parameter for this purpose: Precise measurements of $B$ [2, 3, 4] can be used to derive limits on hypothetical right-handed current ($V + A$) contributions to $\beta$-decay [5, 6, 7] (mediated by new heavy charged bosons $W_{R}$). These can be compared to other indirect measurements in muon [8] and nuclear $\beta$-decay [9] as well as to collider attempts to directly produce the $W_{R}$ [10] (cf. also [11]). When interpreted in general left-right symmetric (LRS) models beyond manifest LRS theory, information from all these experiments (direct, muon, and $\beta$-decay) are complementary and necessary to obtain limits [9].

A deviation from eq. (2) is a sign for new physics not described within the Standard Model and may be due to admixtures of right-handed currents, or due to anomalous (scalar, tensor) couplings possibly caused by exotic models like leptoquark exchange [12]. A recent review on this topic can be found in [13]. Neutron decay, involving all particles of the first generation, is well suited to study the structure of the weak interaction [14] since theoretical corrections are small and well calculable as they do not depend on nuclear structure [13, 16, 17].

In order to measure the neutrino asymmetry parameter $B$, the electron spectrometer PERKEO II [15] was installed at the cold neutron beam position PF1B [19] at the High Flux Reactor of the Institut Laue-Langevin (ILL), Grenoble. A cold neutron beam with a thermal equivalent flux of $1.3 \times 10^{10}$ n cm$^{-2}$ s$^{-1}$ was transversally spin polarized in a system of two supermirror polarizers in the new X-SM geometry [20]. A radiofrequency (rf) spinflipper [21] allowed to reverse the spin direction. Polarization $P$ and spinflipper efficiency $\epsilon$, formerly sources of large corrections and uncertainties, were determined to $P = 0.997(1)$ and $\epsilon = 1.000(1)$ leading to a $0.30(14)\%$ correction on $B$. $P$ and $F$ were measured as a function of the neutron wavelength by a time-of-flight method. A second rf-flipper and two supermirror analyzers in the geometry of [20] were used to determine $F$ and to scan $P$. For the precise measurement of the absolute beam polarization, several opaque polarized $^3$He cells [22, 23] were employed. Both, $P$ and $F$ were uniform over the full neutron beam cross section for all wavelengths. The flipping ratio, a measure for $PF$, was monitored regularly and stayed constant during beamtime.
Since the neutrino cannot be measured directly, electron and proton were detected in coincidence to reconstruct the neutrino. Most sensitive to $B$ is the case when electron and proton are emitted into the same hemisphere relative to the neutron spin – momentum conservation then restricts the neutrino to the opposite direction. The other case, where electron and proton are emitted into different hemispheres, is kinematically favored but less sensitive to $B$ since the neutrino direction is less constrained \[26\]. As it depends strongly on detector calibration, this case was only used for cross checks of the result obtained for the first case.

Electrons ($E_{\text{max}} = 782\) keV) are detected by $190 \times 130 \text{ mm}^2$ plastic scintillators with photomultiplier readout. The protons having much lower energies ($E_{\text{p,max}} = 780\) eV) are accelerated onto a thin carbon foil ($15\sim30 \mu g/cm^2$, coated with MgO) on negative potential ($V = -18\) kV). Whereas the electrons pass the foil almost unperturbed, the heavy protons have enough ionization power to release one or several secondary electrons from the foil \[27\]. These are detected in the scintillator, where also the proton time-of-flight is registered. No precise energy information on the proton is obtained with this method. Proton detection does not depend on the initial proton energy and the angles of incidence occurring in this setup as was experimentally verified.

The measured signature is the experimental neutrino asymmetry defined by

$$B_{\text{exp}}(E) = \frac{N^{--}(E) - N^{++}(E)}{N^{--}(E) + N^{++}(E)}, \tag{3}$$

where $N^{ij}(E)$ is the number of coincident events with electron kinetic energy $E$. The first/second sign indicates whether the electron/proton was emitted in ($+$) or against ($-$) neutron spin direction. Eq. \[8\] is related to the neutrino asymmetry parameter $B$ by integrating eq. \[11\] over the hemisphere \[16, 22\]

$$B_{\text{exp}}(E) = \frac{4 P}{3} \begin{cases} \frac{A \beta (2r^3 - 3) + B (3 - r^2) - 3 \beta + 2 B r}{8 - 4r + A \beta (r^2 - 2)} & [r < 1] \\ - \frac{A \beta + 2 B r}{4 - A \beta} & [r \geq 1]. \end{cases} \tag{4}$$

The definition is separated into two regions by the energy dependent parameter $r = \beta (E + m_e)/(E_{\text{max}} - E)$ which is unity at $E = 236\) keV. $\beta = v/c$. Eq. \[11\] is very sensitive to the coefficient $B$ but also depends slightly on the correlations $a$ and $A$ whose experimental uncertainties have to be considered.

Detector calibration was performed regularly and two-dimensional detector scans were carried out to correct for spatial detector characteristics. Due to the flat spectral shape of $B_{\text{exp}}(E)$ detector calibration imposes only a tiny uncertainty of 0.02% on $B$.

At low electron energies, there is background related to the high voltage (HV) applied on the carbon foils. Above
230–240 keV, however, the measured electron spectra, i.e. $N^{++}(E)$ and $N^{--}(E)$, can be well described by their theoretical expressions, where all fits have only one free parameter, a normalizing factor. An upper limit on remaining background contributions in the fit region was determined from the fit residuals. At lower energies, a satisfactory description is impossible due to background, a non-linear energy calibration, and backscattered electrons assigned to the wrong detector [28].

All corrections due to the spectrometer design have been obtained from Monte Carlo simulations. The “edge effect” accounts for the loss of charged particles due to the finite length of the decay volume that was defined by thick aluminum baffles. “Grid Effect”: Four layers of grids made of AlSi-wires (10 µm and 25 µm) were used to prevent the HV applied to the detector foils to reach into the decay volume. Different methods (finite elements, boundary elements) showed that the absolute electric potential in the decay volume is at least one order of magnitude below a value that would cause systematic effects at the present level of experimental precision. However, electrons and protons may be absorbed or scattered by the grids. This “grid effect” was obtained using the program PENELOP [29] to simulate the electron trajectories in the wires. Protons hitting the wires were assumed to be absorbed. The potential barrier for electrons to reach the scintillator can be neglected since all electrons with $E > 84$ keV will certainly pass it regardless of their initial emission direction.

Charged particles moving in an increasing magnetic field $B^\prime$ may be reflected as $p_\perp^2 / B^\prime$ is an adiabatic invariant, where $p_\perp$ is the momentum component perpendicular to the field lines. This gives rise to the “magnetic mirror effect” since a certain fraction of decay products was emitted towards the field maximum due to the finite neutron beam width. An asymmetric setup, i.e. a displacement $\Delta$ between neutron beam and magnetic field maximum, may cause an additional, possibly large effect on $B$. Therefore $\Delta$ was measured directly and was additionally determined from data in two independent ways to correct for the effect: It was obtained from a $\chi^2$-minimization of fits to the difference spectrum $D(E) = N^{--}(E) - N^{++}(E)$ that has the highest sensitivity on $\Delta$ at high electron energies $E$. $\Delta$ was also determined from the relative difference of the electron asymmetry parameters $A$ measured without ep-coincidence $F(E)$ in eq. (1) has already been corrected for Coulomb interactions $F_C(E)$, proton recoil $R(E)$, and outer radiative corrections $\delta_R(E)$, and reads

$$F(E) = F'(E) \left( 1 + \delta_R(E) \right) \left( 1 + R(E) \right) F_C(E),$$

where $F'(E)$ is the uncorrected phase space factor. The expressions for $\delta_R(E)$ and $R(E)$ were taken from [13] and [31], respectively. The recoil and order-α corrections to $B$ are of order 0.01% [10].

The proton coincidence window $W_1$ was restricted to 40 µs causing a small correction of $-0.05(3)$% to account for slower protons. Accidental coincidences were directly measured with a delayed coincidence technique in a delayed window $W_2$ from 42–82 µs after the initial trigger. In order to avoid suppression of protons by accidental coincidences or background, or suppression of accidental coincidences by preceding signals, up to 32 stops were detected in both detectors. Only events with exactly one stop in the respective window were considered in the analysis since multiple stops are mostly due to background. Events with a stop in $W_1$ and a second (“accidental”) stop in $W_2$ were included in the analysis.

However, this “1 stop” condition causes an overestimation of accidental coincidences since the stop-signal combination “proton and accidental signal” in $W_1$ is removed from the data set, whereas a similar combination does not occur in $W_2$. The available information on all stops allowed to determine the necessary correction directly from the data.

At high electron energies $E$, the fit region is limited as the uncertainty related to the displacement $\Delta$ between neutron beam and magnetic field increases with $E$. At the low energy side, the fit region is limited by the effects mentioned above: Background, non-linear detector response, and wrongly assigned backscatter events.

| Effect [%]               | Detector 1 |        | Detector 2 |        |
|---------------------------|------------|--------|------------|--------|
| Corr.                     | 0.30       | 0.10   | +0.30      | 0.10   |
| Flip Efficiency           | 0.10       | 0.10   | 0.10       | 0.10   |
| Data Set: Statistics      | 1.22       | 0.36   | 1.22       | 0.36   |
| Proton Window             | -0.05      | 0.03   | -0.05      | 0.03   |
| 1 Stop Condition          | -0.24      | 0.06   | -0.13      | 0.03   |
| Background                | 0.10       | 0.08   | 0.10       | 0.08   |
| Detector Calibration      | 0.02       | 0.02   | 0.02       | 0.02   |
| Spectrometer: Edge Effect | -0.16      | 0.05   | -0.16      | 0.05   |
| Grid Effect               | +0.03      | 0.05   | +0.03      | 0.05   |
| Mirror Effect             | +0.44      | 0.05   | +0.44      | 0.05   |
| Displacement $\Delta$     | -0.10      | 0.32   | +0.10      | 0.32   |
| Correlations $A$, $a$     | 0.07       | 0.07   | 0.07       | 0.07   |
| Sum                       | +0.22      | 1.28   | +0.53      | 0.52   |
region was chosen from 250 – 455 keV. The final asymmetry parameter $B$ is independent of this choice as the fit results agree within $±0.3_{\text{stat}}^{+0.3}_{\text{syst}}$ for intervals between 235 and 620 keV (fig. 4.48 in [28]).

Fig. 2 shows the fit of $B_{\exp}$, eq. (4), to all data of detector 2 (proton efficiency about 17%). It yields the neutrino asymmetry parameter $B_2 = 0.9798(36)_{\text{stat}}(36)_{\text{syst}}$. The result of detector 1, $B_1 = 0.9845(120)_{\text{stat}}(36)_{\text{syst}}$, is limited by statistics due to a smaller proton efficiency. This was caused by an inferior foil coating and higher HV background that could not be further suppressed. A detailed compilation of all relevant corrections and errors is given in table I.

In this situation, with two detectors of very different statistical significance, we use the statistical average as the final neutrino asymmetry parameter result

$$B = 0.9802(50) = 0.9802(34)_{\text{stat}}(36)_{\text{syst}}.$$  

(6)

The experiment is limited by statistics and the uncertainty due to the displacement $\Delta$ between neutron beam and magnetic field. With two detectors of equal performance, both errors would be significantly smaller as the influence of $\Delta$ would cancel by calculating the arithmetic mean of $B_1$ and $B_2$.

The second case, electron and proton in opposite detectors, yields results with much larger uncertainties, 1.9% and 3.0% for detector 1 and 2, respectively, dominated by detector calibration. They statistically agree with (3).

Our result (6) has a precision similar to the most precise measurement so far [3] and agrees very well with all results published earlier. It is distinguished, however, as it features several times smaller corrections than competing experiments (0.5%; 1% if absolute numbers are considered, cf. table I). Our result is consistent with the Standard Model expectation, $B_{\text{SM}} = 0.9876(2)$, calculated with the current world average for $\lambda$ from [11] and eq. (2).

By including our result (6), the error of the world average for $B$ reduces by 25%, yielding $\overline{B} = 0.9807(30)$. We apply this value to analyze a manifest LRS model with zero mixing ($\zeta = 0$), following the procedure described in [7] but with only the electron asymmetry parameter $A$ from [11] as further input parameter; $\lambda$ is a free parameter as it may be different from the SM value. We obtain a lower limit $m_{\text{W_R}} > 290.7$ GeV/c$^2$ (90% CL). The rather small improvement of this limit despite the reduced uncertainty of $\overline{B}$ originates from the shift of $\overline{B}$ to a lower value. Due to the controversial neutron lifetime (cf. [11]) we renounce a more elaborated analysis. However, with this controversy being settled, the improved neutrino asymmetry parameter together with other neutron decay data will permit to derive new limits on general LRS models and on scalar and tensor couplings.

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