What causes the absence of pulsations in Central Compact Objects in supernova remnants?

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Abstract Most young neutron stars belonging to the class of Central Compact Objects (CCOs) in supernova remnants do not have known periodicities. We investigated seven such CCOs to understand the common reasons for the absence of detected pulsations. Making use of XMM-Newton, Chandra, and NICER observations, we perform a systematic timing and spectral analysis to derive updated sensitivity limits for both periodic signals and multi-temperature spectral components that could be associated with radiation from hotspots on the neutron star surface. Based on these limits, we then investigated for each target the allowed viewing geometry that could explain the lack of pulsations. We find that it is unlikely (< 10⁻⁶) to attribute that we do not see pulsations to an unfavorable viewing geometry for five considered sources. Alternatively, the carbon atmosphere model, which assumes homogeneous temperature distribution on the surface, describes the spectra equally well and provides a reasonable interpretation for the absence of detected periodicities within current limits. The unusual properties of CCOs with respect to other young neutron stars could suggest a different evolutionary path, as that proposed for sources experiencing episodes of significant fallback accretion after the supernova event.

Key words: methods: data analysis — stars: neutron — X-rays: stars

1 INTRODUCTION

The Central Compact Objects (CCOs) are a handful of young neutron stars, which are found close to the center of young (0.3 – 7 kyr) supernova remnants (SNRs) (see de Luca 2008; De Luca 2017, for reviews). The discovery of these objects is limited by observational technology. CCOs share similar properties, such as the lack of known optical/radio/IR counterparts; their purely thermal-like spectra can usually be described by a two-blackbody model with a temperature of 0.2 – 0.5 keV (De Luca 2017). At present, about ten sources are confirmed members of the class¹. Only for three sources have periodicities been detected in the X-ray band (105 – 424 ms; Zavlin et al. 2000; Gotthelf et al. 2005; Gotthelf & Halpern 2009).

Dedicated campaigns with XMM-Newton and Chandra revealed the very low period derivatives of these three CCOs (8.7 × 10⁻¹⁸ – 2.2 × 10⁻¹⁷ s s⁻¹; Halpern & Gotthelf 2010a; Gotthelf et al. 2013; Halpern & Gotthelf 2015). Under the assumption of the standard magnetic dipole braking model (Ostriker & Gunn 1969), their characteristic ages are within 192 – 301 Myr (Halpern & Gotthelf 2010a; Gotthelf et al. 2013; Halpern & Gotthelf 2015), which implies a factor of about five order magnitudes higher than the estimated age of the associated SNRs (4.5 – 7 kyr; Sun et al. 2004; Becker et al. 2012; Roger et al. 1988). Even though the magnetic field strength of the three CCOs are within 2 × 10¹⁴ G (Gotthelf et al. 2013; Halpern & Gotthelf 2010a, 2015), the anisotropic temperature distributions on the CCOs could be due to localized crustal heating by magnetic decay, which requires a magnetic field strength higher than 10¹⁴ G inside the crustal region (Halpern & Gotthelf 2010a). Alternatively, it may be caused by anisotropic heat transfer from the interior, which also points to the possibility of stronger components of the magnetic field inside the neutron star (Pérez-Azorín et al. 2006; Geppert et al. 2004). A normal magnetic field may be buried inside the core or crust of the neutron star so that a weak magnetic field presents. The buried magnetic field then

¹ See the complete catalog at http://www.iasf-milano.inaf.it/~deluca/cco/main.htm
takes thousands of years to diffuse back to the surface, during which time the neutron star shows a weak magnetic field and with no flux variability, which is so-called “anti-magnetar” (Halpern & Gotthelf 2010a; Gotthelf et al. 2013). Though the most CCOs have low pulsed fractions (see, e.g., de Luca 2008; Halpern & Gotthelf 2010b), the “anti-magnetar” explanation still cannot account for the high pulsed fraction (hereafter, PF) that occurred in Kes 79 (Halpern & Gotthelf 2010a) or the two antipodal hot spots of different temperatures and areas on the CCO in Puppis A (Gotthelf & Halpern 2009) since the weak magnetic fields are not enough to generate the luminosity in X-ray band (Gotthelf et al. 2013).

Alternatively, the carbon atmosphere model, which relies on a uniform temperature distribution on the surface, successfully described the spectrum of the CCO in Cas A and also yielded a neutron star radius expected for nuclear matter (Ho & Heinke 2009; Özel & Freire 2016). This model was also successfully applied to the other CCOs, such as XMMU J173203.3-344518 in G353.6-0.7 (Klochkov et al. 2013) and CXOU J160103.1-513533 in G330.2+10 (Doroshenko et al. 2018). Nevertheless, there is no direct evidence to verify the existence of a carbon atmosphere (Bogdanov 2014; Suleimanov et al. 2017). Notably, Bogdanov (2014) showed that the spectrum of the CCO in Kes 79 can also be well described by a single-temperature carbon atmosphere model despite the high pulsed fraction of the source (64%; Halpern & Gotthelf 2010a).

On the other hand, an unfavorable viewing geometry can also naturally explain the absence of pulsed signals (Suleimanov et al. 2017; Doroshenko et al. 2018; Pires et al. 2019). Although definite conclusions in general cannot be drawn for individual sources, it is possible to estimate the joint probability that we miss modulations for all neutron stars belonging to this class (e.g. Doroshenko et al. 2018). By modeling light curves of three objects, Doroshenko et al. estimated a small joint probability for such a scenario, about 0.3%.

In this work, we analyze seven CCOs without detected periods as a class to investigate the common reasons for the absence of pulsations. We consider the observations operated by XMM-Newton, Chandra, and the Neutron star Interior Composition Explorer (NICER) for more stringent limitations on the pulsed fraction. This paper is organized as follows: In Section 2, we describe the observations and data reduction of XMM-Newton, Chandra, and NICER. We present the data analysis and the results in Section 3. In Section 4, we apply our results to discuss the viewing geometry of the CCOs and the presence of hot spots. We summarize the results and conclusions in Section 5.

\[ PF = \frac{F_{\text{max}} - F_{\text{min}}}{F_{\text{max}} + F_{\text{min}}} \]

where \( F_{\text{max}} \) and \( F_{\text{min}} \) are the maximum and the minimum fluxes.

2 OBSERVATIONS AND DATA REDUCTION

All targets have been repeatedly observed by XMM-Newton (Jansen et al. 2001), Chandra Observatories (Weisskopf et al. 2002) and NICER (Gendreau & Arzoumanian 2017) in several occasions in the past twenty years. Table 1 gives an overview of the datasets included in the analysis, with details of the scientific exposures and corresponding observing modes. For each target we analysed the longest archival observation with as high time resolution as possible, to achieve the most sensitive and constraining limits for the analysis. For Cas A, we did not include the observation operated by XMM-Newton because of heavy contamination from the SNR (≈ 90%), even though it was observed longer and with higher time resolution than before (117 ks; ObsID 0650450201). The observations conducted with the EPIC-pn camera (Strüder et al. 2001) in small-window (SW) and full-frame (FF) imaging mode provide a time resolution of 5.7 ms and 73.4 ms, respectively. In contrast, the time resolution of the EPIC-MOS can only reach 0.3 s in SW mode and 2.6 s in FF mode. The Advanced Camera for Imaging and Spectroscopy (ACIS-S, Garmire et al. 2003) in FAINT and continuous-clocking (CC) mode provide time resolutions of 0.341 s and 2.85 ms, respectively. Moreover, the X-ray Timing Instrument (XTI), NICER’s payload, provides time resolution better than 100 ns (Gendreau & Arzoumanian 2017).

For the NICER observations, we estimated the level of background contamination using PIMMS\(^3\) and the spectral parameters of each CCO determined in previous work. For the CXOU J232327.9+584842 in Cas A, the photon count is dominated by the emission from the SNR (over 99%), so we do not include it in the analysis. Furthermore, we found that the observation of the CXOU J181852.0-150213 provides more photons so that it is possible to get a stringent PF limit than before. Besides, we consider the observation of 1WGA J1713.4-3949 and XMMU J173203.3-344518 here.

For XMM-Newton observations, we performed standard data reduction with SAS version 18.0.0 (xmmmsas20190531_1155-18.0.0) applying the latest calibration files and following the analysis guidelines of the EPIC-pn instrument\(^4\). We processed the exposures using the SAS meta task epproc and applied default corrections. For the Chandra observations, we used ciao 4.12 (Chandra Interactive Analysis of Observations) with the corresponding CALDB version 4.9.2.1 for the data processing. For NICER, standard data reduction was performed with HEAsoft v6.28, using the latest NICER calibration files (version 20200722).

\(^3\) https://heasarc.gsfc.nasa.gov/cgi-bin/Tools/w3pimms/w3pimms.pl
\(^4\) https://xmmweb.esac.esa.int/docs/documents/CAL-TN-0018.pdf
The percentages of good-time-intervals (GTIs), removing the periods of high background or flaring activity, are shown in Table 1. For EPIC-pn, we adopted the standard count rate thresholds (0.4 s\(^{-1}\)) to filter the event lists. We also filtered the event lists to exclude bad pixels and columns and to retain photon patterns with the highest quality energy calibration (for EPIC-pn, \(\text{PATTERN} \leq 4\)). The source centroid and optimal extraction region, optimizing with a high signal-to-noise ratio, were defined in the whole energy band from 0.2 keV to 12 keV. We ensured the choice of background regions avoided as much as possible the contamination from diffuse emission and out-of-time events. We defined background regions of sizes 40\(\arcmin\) to 60\(\arcmin\), away from the source region but on the same CCD as the target. Especially for the observations in SW mode, we verified that the results of the spectral analysis were not significantly affected by the choice of background region or window mode. Besides, we have not included ObsID 0722190201 in the spectral analysis since it is so bright that it is hard to select the background region in the same CCD.

For the Chandra observations, we applied the task chandra_repro to remove hot pixels and background flares. To minimize the contamination from diffuse emission, we optimized the source region with the help of radial profiles, e.g. by defining the extraction radius at the distance from the central target where counts rapidly drop to a near-zero level (e.g., 1.476\(\arcmin\) for J2323). Following Posselt & Pavlov (2018), we chose 2.46\(\arcmin\) < \(r\) < 4.92\(\arcmin\) as the background region of the J2323 and used a box to exclude the apparent filament-like structure around the center. For the data observed in CC mode, we followed the Chandra X-ray Center guidelines\(^5\) and used box-shaped regions to select the source and background regions.

For the NICER observations, the standard NICER pipeline was applied for data reduction, with most filtering criteria chosen at their standard values. The X-ray photons in interested energy bands were selected with the task fselect before performing the spin frequency search.

For the timing analysis, we converted the times-of-arrival (ToA) of the event files to the solar system barycenter using the axbary tool in CIAO and barycen in SAS and the astrometrically corrected coordinates of each target, which is especially important for observations conducted in CC mode. For NICER observations, the ToA of X-ray events were converted to the ICRS reference frame, and the ephemeris was specified to DE200.

To estimate the pile-up effect in XMM-Newton data, we followed the guidelines of Jethwa et al. (2015). For the observations in FF mode, we ensured that the pile-up levels were within conservative thresholds for both the flux loss and spectral distortion (less than 1.0\% and 0.4\%, respectively). The observations conducted in SW mode are not affected by pile-up due to the higher time resolution. For Chandra, the pile-up level estimated by the pileup_map tool\(^6\) can be considered to be overall negligible at the flux level of our targets.

### 3 ANALYSIS AND RESULTS

#### 3.1 Revised Upper Limits on the Neutron Star Spin Period

We applied the \(Z_\text{in}^2\) (Rayleigh) test (Buccheri et al. 1983) directly on the times-of-arrival of the events to search for periodic signals. We can search for periodicity below Nyquist frequency, e.g., \(f_{\text{max}} = 1/(2\text{t}_{\text{res}}) = 87.71\ HZ\), where \(\text{t}_{\text{res}} = 5.7\ ms\) is the time resolution in SW mode. But for the NICER observations, \(f_{\text{max}}\) was set to 50 Hz to save computing time. We set the minimum frequency to

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\(^5\) [https://cxc.cfa.harvard.edu/ciao/caveats/acis_cc_mode.html](https://cxc.cfa.harvard.edu/ciao/caveats/acis_cc_mode.html)

\(^6\) [https://cxc.harvard.edu/ciao/ahelp/pileup_map.html](https://cxc.harvard.edu/ciao/ahelp/pileup_map.html)
does not show pulsation with a pulsed fraction larger than 7% at 99% confidence level. This is consistent with the limit reported by de Luca (2008), that is, less than 7% (99% c.l.) in a period range of 12 ms to 6 s. However, our analysis does not show any significant pulsed signal above 6 ms, and the pulsed fraction above 6% is not larger than 16% (at 3σ confidence level), which is consistent with that derived by Doroshenko et al. (2010a) (< 12%, consistent with that reported by Halpern & Gotthelf (2010a) (PF < 12% above 10 ms, 99% c.l.).

| Targets | ObsID | Energy Band (keV) | Photons | $f_{\text{min}}$ (Hz) | $f_{\text{max}}$ (Hz) | $f_{\text{step}}$ (μHz) | $N_{\text{trial}}$ | PF$_{3\sigma}$ (%) |
|---------|-------|------------------|---------|-------------------------|-------------------------|------------------------|-------------------|------------------|
| J0852   | 0652510101 | 0.5 – 6.0 | 24310 | 0.01 | 87.71 | 4 | | |
| J1601   | 0742050101 | 1.1 – 6.0 | 2457 | 0.01 | 6.81 | 1 | | |
| J1713   | 722190101 | 0.3 – 6.0 | 100950 | 0.01 | 87.71 | 1 | | |
| J1720   | 14806 | 1.0 – 6.0 | 38750 | 0.01 | 50 | 2 | | |
| J1732   | 0722190201 | 1.0 – 6.0 | 44715 | 0.01 | 87.71 | 1 | | |
| J1818   | 16766 | 0.5 – 9.0 | 308 | 0.01 | 0.156 | 2 | | |
| J2323   | 16946 | 0.5 – 8.0 | 5971 | 0.01 | 1.466 | 2 | | |

Notes: PF$_{3\sigma} = (2Z_{1.3\sigma}/N_{\text{photons}})^{1/2}$

In Table 2, we summarize the results of the timing analysis for each target. For J0852, taking into account the number of independent trials (see, e.g., Pavlov et al. 1999), we found no significant pulsations with pulsed fraction above 6% (3σ threshold) in a period range of 12 ms – 100 s range, which is consistent with the limit reported by de Luca (2008), that is, 7% at 99% confidence level.

The analysis of XMM-newton observation for J1601 does not show pulsation with a pulsed fraction larger than 18% (3σ threshold) in a period range of 147 ms to 100 s, which is consistent with that derived by Doroshenko et al. (2018) (< 21%, at the same period range).

Pulsation searches for J1713 yield a pulsed fraction limit of 3% (3σ) down to a pulse period of 12 ms, which is consistent with the limit reported by de Luca (2008), that is, less than 7% (99% c.l.) in a period range of 12 ms to 6 s.

The observation of J1720, performed in continuous-clocking mode, gives us the chance to search for a period above 6 ms. However, our analysis does not show any significant pulsed signal above 6 ms, and the pulsed fraction is no larger than 16% (at 3σ confidence level), coincides with Lovchinsky et al. (2011), that is PF < 16% (at 99% confidence level) in the range above 6.4 s.

Our analysis for J1732 does not reveal any pulsations with pulsed fraction larger than 5% (3σ c.l.) in the 12 ms – 100 s range, which is consistent with the upper limit ~8% down to 0.2 ms at 99% c.l. reported by Klochkov et al. (2013).

For J1818, when we reanalyzed the dataset as Klochkov et al. (2016), we did not find any pulsations (PF < 50%, at 3σ c.l.) in the period range of 6.2 s to 100 s, consistent with the derived 99% c.l. upper limit of 56% reported by Klochkov et al. (2016). The 3σ upper limit using the NICER dataset (including ~ 70% background) is down to 18% in the range of 20 ms – 100 s.

Our analysis of Chandra observation for J2323 in the Cas A has not found any significant periodic signal above 0.68 s. The 3σ confidence level value of the upper limit is 12%, consistent with that reported by Halpern & Gotthelf (2010a) (PF < 12% above 10 ms, 99% c.l.).

### 3.2 Spectral Analysis

We extracted spectra from the source and background regions described in Section 2, together with the respective response matrices and ancillary files created by SAS task rmfgen and arfgen, while these processes were included in the pipeline specrest for Chandra observations. For Chandra observations operated in CC mode, the specrest setting followed the guidelines provided by the CXC\footnote{https://cxc.cfa.harvard.edu/ciao/caveats/acis_cc_mode.html}. For the XMM-Newton observations, the energy channels of each spectrum were regrouped with minimum counts of at least 25 per spectral bin. We ensured the binning does not overample the instrumental energy resolution by more than a factor of 3. The counts in each group were at least 25 for the Chandra observations, except for the observation in CC mode, in which we adopted at least 30 counts/bin. To fit the spectra, we used Xspec version 12.10.1f (Arnaud 1996). In the analysis, we adopted the tbabs model and wilm abundance table in XSPEC (Wilms et al. 2000) to model the interstellar absorption in the line-of-sight. We estimate that the choice of abundance table and cross-section model impacts the results of the spectral fitting by 20% – 30% in column density.

We modeled the thermal spectra of CCOs as single and multi-temperature blackbody components, absorbed by the interstellar material. Since a single blackbody model results in an unrealistic emission radius at a given
Table 3 The Best-fit Results for the Two-component Blackbody Model

| Target            | EB  | $\chi^2_\nu$ | NHP (%) | $n_H$ ($10^{22}\,\text{cm}^{-2}$) | $kT_{\nu}$ (keV) | $R_{\nu}$ (cm) | $kT_{\nu}^n$ (keV) | $R_{\nu}^n$ (cm) | Flux $\times 10^{-18}$ | Notes |
|-------------------|-----|--------------|---------|----------------------------------|------------------|----------------|-------------------|----------------|---------------------|-------|
| J0852             | 0.8-5.0 | 0.87(68) | 77 | 0.55±0.06 | -0.05 | 317±33 | 0.39±0.08 | 0.04 | 452±89 | 0.12±0.07 | 0.06 | 0.00 | 1.34(1) | |
| J1601             | 1.0-6.0 | 1.01(47) | 45 | 4.85±0.65 | -0.04 | 303±67 | 1.41±0.67 | 4.9 | 531±65 | 0.28±0.16 | 0.18 | 0.125(3) | |
| J1713             | 0.4-5.0 | 0.95(92) | 61 | 0.55±0.01 | -0.01 | 343±10 | 0.67±0.02 | 0.01 | 552±10 | 0.17±0.03 | 0.12 | 3.18(12) | |
| J1720             | 0.5-8.0 | 0.83(115) | 90 | 4.67±1.17 | -0.05 | 234±133 | 2.17±10.36 | 0.11 | 511±26 | 0.72±0.15 | 0.125 | 0.49(1) | |
| J1732$^a$         | 0.5-6.0 | 1.25(192) | 1 | 2.19±0.06 | -0.05 | 426±18 | 1.30±0.10 | 0.32 | 688±99 | 0.24±0.13 | 0.10 | 2.66(15) | |
| J2323             | 0.8-6.0 | 0.95(132) | 64 | 1.92±0.17 | -0.23 | 286±63 | 1.49±0.15 | 0.13 | 479±59 | 0.45±0.13 | 0.64 | 0.63(1) | |
| Notes: The model fitted to the data in XSPEC is $\text{TBabs(bbodyrad+bbodyrad)}$. Errors are 1σ confidence levels. | |

Table 4 Results of the Best-fit Three-component Blackbody Model

| Targets | $\chi^2_\nu$ | NHP (%) | $n_H$ ($10^{22}\,\text{cm}^{-2}$) | $kT_{\nu}$ (keV) | $R_{\nu}$ (cm) | $kT_{\nu1}$ (keV) | $R_{\nu1}$ (km) | $kT_{\nu2}$ (keV) | $R_{\nu2}$ (km) | $kT_{\nu3}$ (keV) | $R_{\nu3}$ (km) | Flux |
|---------|--------------|---------|----------------------------------|------------------|----------------|------------------|----------------|------------------|----------------|------------------|----------------|-------|
| J0852   | 0.83 | 83 | 0.94±0.28 | -0.30 | 89±16 | 13 | 243±22 | 0.77±0.26 | 0.33 | 438±12 | 0.20±0.09 | 0.12 | 1.34(11) |
| J1601   | 1.0 | 46 | 5.58±1.25 | -1.26 | 138±26 | 15 | 289±26 | 1.80±0.97 | 0.31 | 526±51 | 0.29±0.16 | 0.125 | 0.49(1) | |
| J1713   | 0.89 | 75 | 0.89±0.03 | 0.05 | 95 | 13 | 267±7 | 1.21±0.06 | 0.1 | 486±10 | 0.30±0.09 | 0.12 | 3.17(12) | |
| J1720   | 1.19 | 4.1 | 2.34±0.11 | -0.05 | 115±19 | 25 | 402±12 | 1.46±0.15 | 0.04 | 643±44 | 0.33±0.12 | 0.12 | 2.66(15) | |
| J2323   | 0.96 | 63 | 2.0±0.4 | 0.00 | 100±13 | 44 | 281±66 | 1.61±0.90 | 0.29 | 479±52 | 0.46±0.12 | 0.18 | 0.63(1) | |
| Notes: The model fitted to the data in XSPEC is $\text{TBabs(2\,bbodyrad+bbodyrad)}$. Errors are 1σ confidence levels. The observed model flux is in units of $10^{-12}\,\text{erg}\,\text{s}^{-1}\,\text{cm}^{-2}$ in energy band 0.5 – 12 keV. | |

Table 5 Results of the Best-fit Carbon Atmosphere Model

| CCO    | $\chi^2_\nu$ | NHP (%) | $n_H$ ($10^{22}\,\text{cm}^{-2}$) | $T$ (MK) | $A$ |
|--------|--------------|---------|----------------------------------|----------|-----|
| J0852  | 0.86 | 79 | 0.70±0.02 | 0.03 | 1.68±0.03 | 0.03 | 1.34(1) |
| J1601  | 0.98 | 51 | 4.71±0.25 | 0.13 | 1.84±0.10 | 0.18 | 0.59(12) |
| J1713  | 0.98 | 55 | 0.71±0.01 | 0.04 | 1.97±0.01 | 0.02 | 0.32(15) |
| J1720  | 0.89 | 80 | 5.74±0.24 | 0.23 | 2.37±0.11 | 0.10 | 0.9(50) |
| J1732  | 1.32 | 0.18 | 2.57±0.03 | 0.01 | 2.92±0.03 | 0.03 | 0.81(265) |
| J2323  | 0.95 | 66 | 2.06±0.00 | 0.06 | 1.9±0.07 | 0.07 | 0.63(1) |

Errors are 1σ confidence levels. \(A\) characterizes the fraction of the surface area emitting the radiation. The observed flux is in unit of $10^{-12}\,\text{erg}\,\text{s}^{-1}\,\text{cm}^{-2}$ in energy band 0.5 – 12 keV.

CNOX J085201.4–461753 We fit the spectra of the CCO J0852 in the SNR G266.2–1.2 (aka Vela Jr.) (2.4 – 5.1 kyr, Pavlov et al. 2001; Kargaltsev et al. 2002; Allen et al. 2015) in the energy range of 0.8 keV to 5.0 keV to minimize the influence of the remnant Vela in the line of sight. The two-temperature blackbody model gives $kT_{\nu} = 317±33$ keV with $R_{\nu} = 0.39±0.08$ km and $kT_{\nu} = 482±85$ keV with $R_{\nu} = 0.12±0.04$ km, where $d_1 = 1$ kpc provided by Allen et al. (2015). The hot-spot in the two-component model also contributes most flux to the spectrum so that the colder surface component is insignificant. Assuming a third blackbody component, we obtain $kT_{\nu} < 89$ keV, which agrees with that derived by Danilenko et al. (90 ± 10 keV; Potekhin et al. 2020).
Table 6 Results of the Best-fit Two-temperature Hydrogen Atmosphere Model

| CCO    | $\chi^2_d$ | NHP (%) | $n_H$ (10^{22} cm$^{-2}$) | $T_1$ (MK) | $T_2$ (MK) | $\delta$ | Flux   |
|--------|------------|---------|--------------------------|------------|------------|----------|--------|
| J0852  | 0.88       | 76      | 0.796$^{+0.067}_{-0.110}$ | 0.82$^{+0.06}_{-0.11}$ | 2.97$^{+0.07}_{-0.06}$ | 0.0063  | 1.332(11) |
| J1601  | 0.99       | 49      | 5.30$^{+0.37}_{-0.40}$    | 1.62$^{+0.10}_{-0.11}$ | 4.11$^{+0.30}_{-0.36}$ | 0.0061  | 0.124(3)  |
| J1713  | 1.31       | 2.2     | 0.71$^{+0.01}_{-0.23}$    | 0.96$^{+0.03}_{-0.01}$ | 3.33$^{+0.07}_{-0.02}$ | 0.0143  | 3.163(12) |
| J1720  | 1.82       | 91      | 5.03$^{+0.50}_{-0.20}$    | 0.34$^{+0.10}_{-0.57}$ | 3.43$^{+0.13}_{-0.04}$ | 0.0402  | 0.497(8)   |
| J1732  | 1.39       | 10$^{-2}$ | 2.62$^{+0.07}_{-0.06}$    | 1.79$^{+0.07}_{-0.09}$ | 4.25$^{+0.11}_{-0.10}$ | 0.0369  | 2.647(15)  |
| J2323  | 0.95       | 65      | 2.12$^{+0.14}_{-0.18}$    | 1.62$^{+0.13}_{-0.23}$ | 3.85$^{+0.30}_{-0.26}$ | 0.0239  | 0.63(1)   |

Notes: Errors are 1σ confidence levels. Here 0 ≤ δ ≤ 1 is defined by the fraction of the surface area occupied by the hot-spots. The observed flux is in unit of 10$^{-13}$ erg s$^{-1}$ cm$^{-2}$ in energy band 0.5 – 12 keV.

Table 7 The Best-fit Results of J1818

| Param. | Model | bbodyrad | hatm | carbatm |
|--------|-------|----------|------|---------|
| $n_H$ (10^{22} cm$^{-2}$) | 3.6$^{+1.1}_{-1.0}$ | 4.2$^{+1.2}_{-1.1}$ | 5.1$^{+1.2}_{-1.2}$ |
| T(MK) | 5.7 ± 0.6 | 3.9 ± 0.6 | 2.0 ± 0.5 |
| D(kpc) | 295$^{+33}_{-29}$ | 74$^{+50}_{-31}$ | 16$^{+20}_{-14}$ |
| $\chi^2_{red}$(d.o.f.) | 0.61(10) | 0.59(10) | 0.58(10) |
| Flux | ~ 3.2(4) × 10^{-14} erg s^{-1} cm^{-2} |

Notes: Errors are 1σ confidence levels. The observed flux is in unit of 10$^{-12}$ erg s$^{-1}$ cm$^{-2}$ in energy band 0.5 – 12 keV.

For the atmosphere models with canonical mass and radius, the best-fit distance for the carbatm model is about 2.5 kpc, which is higher than that estimated for G266.2-1.2 Allen et al. (2015). Similar results are obtained for the two-component hatm model (Table 6). The best-fit column density in the direction to the source (0.7 – 0.8) × 10^{22} cm$^{-2}$ agrees to that derived for G266.2-1.2 (< 1.1 × 10^{22} cm$^{-2}$; Slane et al. 2001; Acero et al. 2013; Allen et al. 2015).

For the atmospheric models with fixed neutron star mass and radius, the best-fit distance for the carbatm model is about 2.5 kpc, which is higher than that estimated for G266.2-1.2 Allen et al. (2015). Similar results are obtained for the two-component hatm model (Table 6). The best-fit distance for G266.2-1.2 (< 1.1 × 10^{22} cm$^{-2}$; Slane et al. 2001; Acero et al. 2013; Allen et al. 2015).

CXOU J160103.1-513353 The CCO J1601 in the SNR G330.2+1.0 (1 kyr, Borkowski et al. 2018) is located at least 4.9 ± 0.3 kpc away from Earth (McClure-Griffiths et al. 2001). Its age, estimated from the decelerated expansion of the associated SNR, is younger than 1 kyr (Borkowski et al. 2018). Using a two-component blackbody model, the temperature of the cool and hot components are 303$^{+84}_{-67}$ eV and 531$^{+150}_{-55}$ eV, corresponding to radiation radius of 1.41$^{+2.23}_{-1.05}$ km and 0.28$^{+0.10}_{-0.14}$ km respectively. The upper limit on the temperature of a cold surface is $kT_{\infty}^c < 138$ eV, which is consistent with that presented by Doroshenko et al. (2018), using the carbon atmosphere model.

Regarding atmosphere models, both the carbon and two-component hydrogen atmospheres describe the data well. However, as discussed by Doroshenko et al. (2018), the both models require a higher absorption column density than that derived for G330.2+1.0 ($n_H \leq 3.15 \times 10^{22}$ cm$^{-2}$; Williams et al. 2018). The distance assuming radiation from the whole neutron star surface is 6.38$^{+1.07}_{-1.35}$ kpc for the carbatm model, which coincides with the lower limit of 4.9 ± 0.3 kpc derived by McClure-Griffiths et al. (2001). Even though none of the atmosphere models is preferred, the hot-spot contributes more than 69% flux in the energy band of 0.5 keV to 10 keV, which may mean that the cool component is not significant for the fit. This is in line with the results of Doroshenko et al. (2018) and Park et al. (2009).

1WGA J1713.4–3949 The CCO J1713 in the SNR G347.3–0.5 (~ 1.6 kyr, Slane et al. 1999; Lazendic et al. 2003; Wang et al. 1997) is located 1.3 ± 0.4 kpc away from the observer (Cassam-Chenaï et al. 2004). The double-blackbody (2BB) model fit to the spectrum of the source gives $kT_{\infty}^c = 343^{+10}_{-11}$ eV, $R_{\infty}^c = 0.67^{+0.02}_{-0.02}$ $d_{1.3}$ km for the cold component and $kT_{\infty}^h = 552^{+30}_{-24}$ eV, $R_{\infty}^h = 0.17^{+0.03}_{-0.03}$ $d_{1.3}$ km for the hot component, where $d_{1.3}$ is the distance in units of 1.3 kpc (Cassam-Chenaï et al. 2004). If we assume the emission from the colder neutron star surface is absorbed by the high Galactic absorption, we obtain an upper limit $kT_{\infty}^c < 95$ eV for $R_{\infty}^c = 15.1$ $d_{1.3}$ km (see Table 4), which is more acceptable for a young (e.g., $10^3 - 10^4$ yr) cooling neutron star (< 90 – 110 eV, assuming standard cooling for a canonical neutron star, Yakovlev & Pethick 2004). By comparison, Potekhin et al. (2020) gave a value of 138 ± 1 eV using atmosphere model (TBabs+NSX).

The fit of atmosphere models with fixed neutron star mass and radius, 1.5 $M_\odot$ and 12 km, respectively, have a $\chi^2_{\nu} = 0.98$ for carbatm and $\chi^2_{\nu} = 1.3$ for a two-component hatm model. The fraction of the emitting area is about 0.2 at a fixed distance of 1.3 kpc. If we assume the radiation arises from the whole surface, the distance to the source is 2.88$^{+0.07}_{-0.07}$ kpc (at 99% confidence level), which is consistent with that derived for G347.3–0.5. Alternatively, the fit with free mass and radius for a source at a distance of 1.3 kpc gives best-fit parameters 0.66 $M_\odot$ and 7.1 km, overall inconsistent with nucleonic matter (Özel & Freire 2016).

XMMU J172054.5–372652 The CCO J1720 associated with the SNR G350.1–0.3 (~ 1 kyr), which is 4.5 kpc away from observer (Gaensler et al. 2008; Lovchinsky et al. 2011). Both single and double blackbody/hydrogen
atmosphere models provide statistically acceptable fit results. The $\chi^2_{\nu}$ values are within 0.8 to 0.9 (d.o.f 115).

The absorption column density of $(4.5 - 5.0) \times 10^{22}$ cm$^{-2}$ is a factor of 0.2 – 0.3 higher than that derived by Gaensler et al. (2008) and Lovchinsky et al. (2011).

If we only consider a single temperature model – for instance, the blackbody model – the emitting area is about 0.7 $d_{4.5}$ km at a distance of 4.5 kpc (Gaensler et al. 2008). Emission from the entire surface is inconsistent with a source located in the Milky Way. The temperature of 0.5 keV is considerably higher than that expected ($< 90$ eV, assuming standard cooling curve by Yakovlev & Pethick (2004)) for a young NS of $\sim$ 0.9 kyr. In comparison, the carbon atmosphere model provides good fits with a colder temperature of 2.37$^{+0.11}_{-0.10}$ MK at a distance of 4.74$^{+0.71}_{-0.71}$ kpc, consistent with that measured for the SNR (Gaensler et al. 2008). However, the model requires a higher absorption column density of $5.74^{+0.21}_{-0.23} \times 10^{22}$ cm$^{-2}$ than the simple blackbody and power-law model (Lovchinsky et al. 2011) to describe the emitted spectrum. This may indicate another absorption component in the line of sight.

**Table 8 Parameters for Each Target Assuming 3-BB Model**

| Target     | $n_H$ (10$^{22}$ cm$^{-2}$) | $kT_1$ (eV) | $kT_{h1}$ (eV) | $\theta_{sp1}$ (°) | $kT_{h2}$ (eV) | $\theta_{sp2}$ (°) | $M_{\odot}$ | $R_{\Delta}$ (km) | $R_{/r_g}$ |
|------------|-----------------------------|-------------|----------------|---------------------|----------------|---------------------|------------|-------------------|-----------|
| J0852      | 99.19                       | 88.6        | 243.5          | 3.39                | 437.8          | 0.86                | 1.5        | 15.1              | 2.71      |
| J1601      | 555                         | 136.65      | 289.1          | 7.0                 | 526.3          | 1.1                 | 1.5        | 15.1              | 2.71      |
| J1713      | 88.53                       | 95.06       | 265.95         | 4.6                 | 486            | 1.13                | 1.5        | 15.1              | 2.71      |
| J1732      | 233.8                       | 115         | 402.2          | 5.51                | 643            | 1.23                | 1.5        | 15.1              | 2.71      |
| J2323      | 201                         | 101.5       | 280.9          | 6.89                | 479.4          | 1.95                | 1.5        | 1.647             | 2.124     |

**Table 9 Probability for Each Target in ‘ad-hoc’ and ‘crustal’ Model**

|           | 'ad-hoc' (%) | 'crustal' (%) |
|-----------|--------------|---------------|
| J0852     | 1.7          | 4.24          |
| J1601     | 90           | 14.8          |
| J1713     | 11.2         | 1             |
| J1732     | 0.4          | 0.4           |
| J2323     |              | 28.4          |

Notes: The probabilities for each object are given in %. The joint probability is shown in the last column in %.

CXOU J232327.9+584842 The CCO J2323 in Cas A, one of the youngest known neutron stars (Ashworth 1980; Fesen et al. 2006), is located at a distance of 3.4 kpc (Reed et al. 1995). The best-fit 2BB model has temperatures and radii of $R_{\Delta} = 1.49^{+0.15}_{-0.51} d_{3.4}$ km and $749^{+59}_{-28}$ eV ($R_{\Delta} = 0.45^{+0.13}_{-0.09} d_{3.4}$ km). If arising from hot spots on the surface, the thermal components contribute the most flux to the source luminosity. Adding a third component to the blackbody model, we find an upper limit of the cold component of $kT_{\Delta} < 124$ eV, which is consistent with the value of $123 - 185$ eV from Wijngaarden et al. (2019) and Heinke & Ho (2010).

The spectrum of J2323 can also be well described by the carbon atmosphere model (Ho & Heinke 2009). In our analysis we assumed the mass and radius of 1.647 $M_{\odot}$ and 10.33 km, respectively, from Posselt et al. (2013). The column density agrees with that derived for the 2BB model (Table 5; see also Posselt & Pavlov 2018) but is a bit higher than that reported by Ho & Heinke (2009). This is likely due to the different adopted abundance tables.

CXOU J181852.0–150213 The CCO J1818, associated with the SNR G15.9+0.2 (3 – 6 kyr), is located at a distance of 8.5 – 16 kpc (Reynolds et al. 2006; Sasaki et al. 2018). The best-fit results are presented in Table 7. All of the tested models provide acceptable fits to the data given the low photon statistics. While the hydrogen column density from both the blackbody and hydrogen atmosphere models is consistent with that measured for the SNR (Klochkov et al. 2016), the distance is 1 – 2 orders of magnitude larger than its expected range, 8.5 – 16.7 kpc (Reynolds et al. 2006; Caswell et al. 1982; Sasaki et al. 2018). By contrast, the carbon atmosphere model gives a consistent distance of $16^{+9}_{-6} \times 10^{28}$ km in general agreement with the SNR (Reynolds et al. 2006; Sasaki et al. 2018). In addition, compared with other models, the temperature ($\sim 170$ eV) given by the carbon atmosphere model is more consistent with that estimated by the standard cooling model, which should be within 110 eV.
4 DISCUSSION

The temperature on the neutron star surface is expected to vary for magnetic field intensities higher than $10^{12}$ G. The heat conduction perpendicular to the magnetic field decreases while it increases along the field lines (Greenstein & Hartke 1983). Furthermore, strong crustal fields ($B > 10^{12}$ G) lead to a highly anisotropic surface temperature variation (Geppert et al. 2004).

A single-component blackbody model cannot describe the spectrum of CCOs. Additional thermal components may closely characterize the spectrum. However, the obtained radii of emitting areas for cold components are ridiculous for a neutron star if we assume the hot component corresponds to the tiny hot-spot region. Here we attempt to assume a three-component blackbody model to investigate the viability of the hot-spot model in CCOs with no detected pulsations.

4.1 The Viewing Geometry and Presence of Hot-spots

The observed pulsed fraction depends on the geometrical configuration of the hot spots and the angle between the neutron star spin axis and the line of sight, which has been discussed by e.g., Elshamouty et al. (2016) for the X-ray binaries and Suleimanov et al. (2017) for CCOs. Strong flux modulations are observed when the rotating axis misaligns with the line of sight. For sources with no detected periodicities, the limits on the pulsed fraction can be used to constrain the viewing geometry assuming the multi-temperature spectral model.

Here we considered the model of a slowly rotating neutron star observed at an inclination angle $i$ with two polar hot-spots located at an angle $\theta_B$ concerning the spin axis (see, e.g., Schwote et al. 2005; Suleimanov et al. 2010; Pires et al. 2019, for a full description). The light bending near the surface depends on the compactness of the neutron star, which is described by Beloborodov (2002) (the ratio between the neutron star and Schwarzschild radius is $r_g = R_{\text{ns}} c^2 (2GM_{\text{ns}})^{-1}$).

The hot-spot model applied to the best-fit two-component blackbody model results in small pulsed fractions, whatever in which angle to observe, smaller than the upper limits derived in timing analysis, which may imply a nearly homogeneous temperature distribution for all the investigated targets. Therefore, we adopted the parameters of the three-component blackbody model (Table 4) and assumed two hot spots with different temperatures and emitting areas located diametrically opposed to each other (hereafter, the “ad-hoc” model). We also applied a variant of the model where the temperature profile is assumed to follow that of Geppert et al. (2004) (hereafter, the “crustal” model).

In the following Table 8, we list all parameters applied to the light-curve modeling process assuming a three-component blackbody model. $T_c$ represents the temperature of the whole cool surface, while $T_{h1}$ and $T_{h2}$ are the temperatures of the hot spots, corresponding with the hot-spot size $\theta_{sp1}$ and $\theta_{sp2}$, respectively. Moreover, the spectral analysis in Section 3.2 gave the absorbed column density. We did not include the analysis of J1818 since we did not get an acceptable result with a multi-component model for poor statistic photons.

We integrate the photon flux originating from the visible area of the neutron star surface for a particular viewing geometry ($i$, $\theta_B$), assuming blackbody emission and considering the light-bending (Beloborodov 2002). Moreover, we also take the interstellar absorption into consideration to correct the actual flux from the surface. Furthermore, the absorption was then folded with the EPIC-pn response to give the computed count rates at a given energy band, while the energy band was given in Table 3. We created a grid of light curves for ($i$, $\theta_B$) within $(0^\circ, 0^\circ)$ and $(90^\circ, 90^\circ)$ and computed the pulsed fraction for each orientation as $PF = \frac{CR_{\text{max}} - CR_{\text{min}}}{CR_{\text{max}} + CR_{\text{min}}}$. The results are presented in Figures 1 and 2. We plot the obtained $PF$ in the ($i$, $\theta_B$) plane and indicate the equal $PF$ with contours. The regions permitted by the observations are shown in pink.

By integrating all possible random orientations of line-of-sight inclination and spot angles where the calculated pulsed fraction is smaller than the upper limit from the timing analysis, we obtain the probability that the absence of pulsed signals is due to an unfavorable viewing geometry (e.g., Suleimanov et al. 2017). For the ‘ad-hoc’ and ‘crustal’ models, we present the calculated probabilities in Table 9, and the probabilities are given in %. As discussed by Doroshenko et al. (2018) and Suleimanov et al. (2017), the probabilities of unfavorable viewing geometry are nonnegligible but relatively small for considering all sources, such as the CCO in SNRs Cas A (J2323), HESS J1731-347 (J1732), G330.2+1 (J1601). Taking these three CCOs in consideration, the probability is about 0.3% (Doroshenko et al. 2018). While we cannot exclude the presence of hot spots individually for sources with poorly constrained pulsed fractions (e.g., $PF < 3\%$ for J1713, and 5% for J1732, see Table 2). As Doroshenko et al. (2018) and Suleimanov et al. (2017) did, we can compute the joint probability that the non-detection of pulsations in all five CCOs is due to unfavorable viewing geometries, assuming that the multi-temperature model is correct. Considering the results for both the ‘ad-hoc’ and ‘crustal’ models (Table 9), this number is quite small, less than $10^{-6}$. This conclusion seems robust against the multi-temperature emission model (see, e.g., Doroshenko et al. 2018).
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4.2 The Carbon Atmosphere

The inferred emission radii in the investigated targets (see Table 3 in Sect. 3.2) are within 0.1 to 1.5 km for a two-blackbody model, smaller than the canonical radius of a neutron star (10 − 15 km, Özel & Freire 2016). Two hot spots with different sizes and temperatures could be responsible for most of the measured flux in these sources. In this case, a third blackbody component (95 − 138 eV, except for J1720 and J1818) representing the colder surface can be added to the model, which may be absorbed by the high hydrogen column density towards the targets ($n_H = 0.5 − 5.0 \times 10^{22}$ cm$^{-2}$). We verified in Section 4.1 that such a description would give rise to significant pulsed fractions (20% − 50%), which, for most cases, could only be missed by the current generation of X-ray observatories for a few possible viewing geometries (Figs. 1 and 2, Table 9).

If the absence of pulsations in most CCOs cannot be simply attributed to an unfavorable viewing geometry, we shall favour an intrinsically homogeneous temperature distribution on the neutron star surface. As discussed by Ho & Heinke (2009), for a neutron star with a carbon atmosphere, the X-ray emission could originate from the entire surface as the star rotates, despite local anisotropies.

Such a model has successfully described the spectrum of the CCOs J1732, J1601 and J1818 (see also Klochkov et al. 2015; Doroshenko et al. 2018; Klochkov et al. 2016). In this work, we also applied it to J1720, J1713, and J0852. We found the carbon atmosphere model characterize their spectra well, with $\chi^2_\nu \sim 0.9 − 1.3$. Moreover, the obtained temperature, 145 − 200 eV, is more acceptable than the single or double component blackbody model for such a young neutron star, assuming the standard cooling model (< 90 − 110 eV, Yakovlev & Pethick 2004), even though the derived distances of J1713 and J0852 are slightly higher than expected of the associated SNR by a factor of 2 − 3. Nevertheless, only the carbon atmosphere model yields an acceptable distance for J1818, as discussed by Klochkov et al. (2016).

The presence of a carbon atmosphere could be understood within the context of hypercritical fall-back accretion and the “hidden” magnetic field model for CCOs (see, e.g., Geppert et al. 2004; Chevalier 1993). Lacking intense magnetospheric activity and pulsar wind nebulae suggest a weak magnetic field on the surface (Ho & Heinke 2009). However, the strong magnetic field buried underneath the deep surface could be possible but has not yet emerged (Muslimov & Page 1995). The hypercritical accretion would submerge the magnetic field soon after the supernova explosion, and the magnetic field is expected to diffuse back to the surface as the accretion weakens (Chevalier 1989; Muslimov & Page 1995). This
re-diffusion process would happen on the time-scale of $10^3 \sim 10^4$ yr (Geppert et al. 1999). For comparison, those CCOs without detected periods have an age range from 0.3 – 6 kyr (e.g., J1713 with an age of $\sim 1.6 - 2.1$ kyr, Tsuji & Uchiyama 2016; J1720 with an age $< 0.6$ kyr, Borkowski et al. 2020), while the ages of CCOs with known periods are range from 4.5 kyr (Becker et al. 2012) to 7 kyr with an uncertainty factor of 3 (Roger et al. 1988). By comparing their ages, the CCOs with no periods detected may be undergoing re-diffusion progress of the magnetic field.

Ho (2011) noted that, for three CCOs with measured spin periods, the bolometric luminosity is higher than its spin-down power of a factor of 3–5, even up to thousands. It could be understood as it is possible to submerge a higher magnetic field underneath the surface by accretion so that to explain the slow period derivatives. On the other hand, accretion is a way to support the relatively higher luminosity if the periodic characteristics could be extend to those CCOs with no periods detected. As discussed by Doroshenko et al. (2016), the brightest known CCO J1732 (up to $10^{34}$ erg s$^{-1}$) could be indirectly explained by powerful accretion when it was born in a binary system. In addition, assuming the gravitational energy of the infalling matter (i.e., $GM\dot{M}/R_{ns}$) is responsible for the luminosity, it implies that an accretion rate larger than $10^{-13}$ $M_\odot$ yr$^{-1}$ could account for the relatively steady X-ray emission of a magnitude of $10^{33}$ erg s$^{-1}$. This rate could be expected to reach $10^{-3}$ $M_\odot$ yr$^{-1}$ in a common envelope (Chevalier 1993), or $10^{-4}$ $M_\odot$ yr$^{-1}$ in the early stage of supernova explosion (Chevalier 1989). Therefore, accretion could be a possible way to explain the slow spin-down characteristic and the corresponding bolometric luminosity.

Moreover, a higher column density obtained for the CCOs applying with the carbon atmosphere model, comparing with the extended emission around the CCOs, may imply an additional absorption component in the line of sight, which has been discussed by Doroshenko et al. (2018) for the CCOs J1601 and J1732. An additional absorption, even up to 20%-30%, may be due to the existence of, e.g., inflow materials or surrounding remnants. An interaction is expected for the CCOs and the surrounding dust shell so that additional enhanced heating of the dust could be observed in the infrared band (Doroshenko et al. 2016). Even though there is no direct evidence for the existence of surrounding material, an
additional component seems like a natural way to explain the relatively higher column density in atmosphere models.

Finally, Ho et al. (2021) also noted that, for the CCO J1713, the slowly increasing magnetic field could be the reason for the gradual increase in temperature. Meanwhile, gravitational wave searches detected an outlier signal of J1713, which may imply a surface magnetic field of \( \sim 6 \times 10^{11} \) G (Papa et al. 2020), though it is higher than three detected CCOs. The magnetic field evolution of the CCOs can be understood with the above scenario, where a strong magnetic field is submerged underneath the surface soon after being born and then back to it with a timescale of \( 10^3 \sim 10^4 \) yr (e.g., Ho 2011; Geppert et al. 1999, 2004; Pons et al. 2009; Perna et al. 2013).

5 CONCLUSIONS

We have conducted a systematic analysis on existing XMM-Newton, Chandra, and NICER observations of seven CCOs in SNRs to investigate the reasons behind their lack of detected pulsations. Compared to previous works, we improved limits on the pulsed fractions of 1WGA J1713.4–3949, XMMU J173203.3–344518, and XMMU J172054.5–372652. We used a multi-component blackbody and atmosphere model to fit the spectra of seven CCOs, and it is hard to determine which one is better based on similar \( \chi^2 \). A third blackbody component is necessary to make it more natural and reasonable, even though the flux contribution of the third component seems negligible. Meanwhile, whether it is the cooler component of the 3-bb model or the carbon atmosphere model, the temperature obtained is consistent with that derived when we assume the standard cooling of young neutron stars. Furthermore, the updated limits and spectral properties of the sources were used to investigate the viability of multi-temperature emission models and the presence of hot spots. The possibility that all five CCOs (except for J1818 and J1720) have unfavorable viewing geometry is relatively tiny (less than \( 10^{-6} \)), which seems impossible. While missing pulsations for individual CCOs in this group could be explained by this process, it is unlikely for all of these CCOs.

Alternatively, the carbon atmosphere model can describe the emission spectra of CCOs and derive a more reasonable emission radius than the blackbody model. The obtained temperature also approaches the value given by the standard cooling curve for young neutron stars. Compared to the inferred emission radius of the two-blackbody model (0.1 – 1.5 km), the emission size derived from the carbon atmosphere model close to a classical neutron star. While notably, the distance derived for 1WGA J1713.4–3949 and CXOU J085201.4–461753 mismatch with previous work and is a factor of 2 – 3 higher than the associated SNRs. While there is no direct evidence of the heavier elements on the surface, the model provides more possibility to explain their spectra. Moreover, the occurrence of carbon on the surface could result from fallback accretion after the supernova explosion, which needs more observations to investigate.

No matter in what scenarios, the absence of pulsations cannot simply be attributed to unfavorable viewing geometry or homogeneous temperature distribution. Both of them may contribute to the absence of pulsation jointly. The fallback accretion, however, could also lead to the inhomogeneous temperature distribution on the surface and further pulsation as the neutron star rotates. In contrast, the unfavorable viewing angles would reduce the observable pulsed fraction. While in this case, further searches are necessary to constraint the upper limits and even the composition on the surface.

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