THE MAIN SEQUENCES OF STAR-FORMING GALAXIES AND ACTIVE GALACTIC NUCLEI AT HIGH REDSHIF'T

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ABSTRACT

We provide a novel, unifying physical interpretation on the origin, average shape, scatter, and cosmic evolution, for the main sequences of star-forming galaxies and active galactic nuclei (AGNs) at high redshift $z \gtrsim 1$. We achieve this goal in a model-independent way by exploiting: (i) the redshift-dependent star formation rate functions based on the latest UV/far-IR data from HST/Herschel, and related statistics of strong gravitationally lensed sources; (ii) deterministic evolutionary tracks for the history of star formation and black hole accretion, gauged on a wealth of multiwavelength observations including the observed Eddington ratio distribution. We further validate these ingredients by showing their consistency with the observed galaxy stellar mass functions and AGN bolometric luminosity functions at different redshifts via the continuity equation approach. Our analysis of the main sequence for high-redshift galaxies and AGNs highlights that the present data are consistently interpreted in terms of an in situ coevolution scenario for star formation and black hole accretion, envisaging these as local, time-coordinated processes.

Key words: galaxies: evolution – galaxies: formation – quasars: general

1. INTRODUCTION

Understanding the coevolution of galaxies and supermassive black holes (BHs) through cosmic times is one of the hottest and most pressing issues of modern research in astrophysics and cosmology.

That some degree of coevolution must be present has been classically established by observing tight relationships between central BH masses and host galaxy properties, such as stellar mass in old stars, luminosity, velocity dispersion, morphological indicators (e.g., Kormendy & Richstone 1995; Magorrian et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000; Tremaine et al. 2002; Marconi & Hunt 2003; Haring & Rix 2004; McLure & Dunlop 2004; Ferrarese & Ford 2005; Graham 2007; Greene & Ho 2007; Lauer et al. 2007; Gültekin et al. 2009; Kormendy & Bender 2009; Vika et al. 2009; Graham et al. 2011; Beifiori et al. 2012; Sani et al. 2012; Kormendy & Ho 2013; McConnell & Ma 2013; Ho & Kim 2014; Shankar et al. 2016), and by recognizing a parallel evolution of the star formation rate (SFR) density for galaxies and of the luminosity density for active galactic nuclei (AGNs; e.g., Boyle & Terlevich 1998; Franceschini et al. 1999; Heckman et al. 2000; Marconi et al. 2004; Silverman et al. 2009; Madau & Dickinson 2014; Aird et al. 2015).

From a theoretical viewpoint, N-body simulations (e.g., Diemand et al. 2007; Springel et al. 2008; Tinker et al. 2008; Stadel et al. 2009) have been extremely successful in accounting for the large-scale matter distribution in the universe as determined by the primordial dark matter perturbations evolving into bound, virialized structures (“halos”) under the action of gravity. However, on smaller, (sub-)galactic scales, the complexity of baryonic physics takes over, making it extremely difficult to provide an ab initio description of all the relevant processes associated to star formation and BH accretion, that occur on vastly different spatial and timescales. This has been demonstrated by the poor predictive capability of current approaches (see Frenk & White 2012; Scannapieco et al. 2012; see the review by Somerville & Davé 2015) based on hydrodynamic codes (e.g., Dubois et al. 2014; Vogelsberger et al. 2014; Khandai et al. 2015; Schaye et al. 2015; Kaviraj et al. 2016; Richardson et al. 2016) or on (semi-)analytic models (e.g., Bower et al. 2006; Croton et al. 2006, 2016; Fanidakis et al. 2011; Guo et al. 2011; Menci et al. 2012; Somerville et al. 2012, 2015; Lacey et al. 2016).

Such difficulties of theoretical models have originated a long-standing debate concerning the main actors in regulating galaxy and BH coevolution. Three popular scenarios are currently (still) on the market. The first one relies on a prominent role of merging among dark matter halos and associated baryons as the main driver of galaxy and BH evolution; specifically, it envisages merging of gas-rich spirals at high redshift as the main route toward building up massive ellipticals and triggering their star formation and BH activity (e.g., Bower et al. 2006; Croton et al. 2006; Hopkins et al. 2006; Fanidakis et al. 2012; Somerville & Davé 2015; Guo et al. 2016). An alternative view assumes that star formation and BH accretion are supported by steady cold gas streams along filaments of the cosmic web (e.g., Dekel et al. 2009; Bournaud et al. 2011). Finally, another view envisages star formation and BH accretion in galaxies to be essentially in situ, time-coordinated processes (e.g., Lapi et al. 2006, 2011, 2014, also Lilly et al. 2013; Aversa et al. 2015; Mancuso et al. 2016), triggered by the early collapse of the host dark matter halos, but subsequently controlled by self-regulated baryonic physics and in particular by energy feedback from supernovae (SNe) and AGNs.
The Astrophysical Journal, 833:152 (15pp), 2016 December 20

Mancuso et al.

The latest interpretation has recently received robust support from observations of high redshift $z \gtrsim 1$ dusty star-forming galaxies, an abundant population discovered via wide areas far-IR/(sub-)mm surveys with Herschel, SPT, LABOCA, and SCUBA2, in many instances thanks to strong gravitational lensing by foreground objects. Specifically, high-resolution follow-up observations of these galaxies in the far-IR/(sub-)mm/radio band via ground-based interferometers, such as SMA, VLA, PdBI, and recently ALMA, have revealed star formation to occur in a few collapsing clumps distributed over spatial scales smaller than a few kpc, and at an overall efficiency lower than 20% (e.g., Finkelstein et al. 2013; Negrello et al. 2014; Neri et al. 2014; Rawle et al. 2014; Riechers et al. 2014; Dye et al. 2015; Ikarashi et al. 2015; Ma et al. 2015a; Simpson et al. 2015; Dunlop et al. 2016; Harrison et al. 2016; Scoville et al. 2016).

Moreover, observations of dusty star-forming galaxies in the optical and near/mid-IR band from archival data and from the Spitzer space observatory have allowed us to characterize their stellar masses. The vast majority of them feature masses strongly correlated to the SFR, in the way of an almost linear relationship dubbed “Main Sequence,” with a normalization steadily increasing as a function of redshift, and with a limited scatter around 0.3 dex (Daddi et al. 2007; Elbaz et al. 2007; Pannella et al. 2009, 2015; Rodighiero et al. 2011, 2014; Speagle et al. 2014; Whitaker et al. 2014; Renzini & Peng 2015; Salmon et al. 2015; Tasca et al. 2015; Dunlop et al. 2016; Erfanianfar et al. 2016; Kurczynski et al. 2016; Martis et al. 2016; Schreiber et al. 2016; Tomczak et al. 2016). In addition, the average dust and molecular gas content of main sequence galaxies (Scoville et al. 2014, 2016; Béthermin et al. 2015) is found to be consistent with the local, integrated Schmidt–Kennicutt diagram (SFR versus mass of molecular gas). All these findings strongly favor in situ star formation by secular processes over the classical merger-driven scenario, and over streamed gas accretion from cosmological scales. A caveat is that an appreciable fraction of galaxies feature SFRs well above the main sequence (Rodighiero et al. 2011, 2015; Silverman et al. 2015), a fact often interpreted as evidence of starbursts triggered by mergers or external inflows; however, we shall show that recent observational evidence on the young age of these systems (e.g., da Cunha et al. 2015; Ma et al. 2015b) points toward an alternative interpretation in line with the in situ scenario.

Recent, model-independent statistical analysis via the continuity equation and the abundance matching techniques (see Moster et al. 2010, 2013; Peng et al. 2010; Behroozi et al. 2013; Aversa et al. 2015; Caplar et al. 2015; Mancuso et al. 2016) have demonstrated that dusty star-forming galaxies with SFRs $\gtrsim 10^2 M_\odot$ yr$^{-1}$ constitute the progenitors of passively evolving systems with large stellar masses $M_\star \gtrsim 10^{11} M_\odot$, that are indeed found to be abundant even at high redshift $z \gtrsim 1$ (see Santini et al. 2012a; Bernardi et al. 2013; Ilbert et al. 2013; Duncan et al. 2014; Tomczak et al. 2014; Caputi et al. 2015; Mawatari et al. 2016; Song et al. 2016). Since massive objects are thought to become passive when their star formation is quenched by the energetic feedback from the central supermassive BH, an exciting bridge between the astrophysics of galaxies and AGNs is naturally established (see Silk & Rees 1998; Fabian 1999; King 2003; Granato et al. 2004; Di Matteo et al. 2005; Lapi et al. 2006, 2014; for a recent review see King 2014).

From this point of view, a great impulse in the study of the role played by supermassive BHs in galaxy evolution has come from: (i) X-ray followup observations of AGNs growing at the center of star-forming galaxies selected in the far-IR/(sub-)mm or in the K-band (e.g., Alexander et al. 2005, 2008; Borys et al. 2005; Laird et al. 2010; Symeonidis et al. 2010; Xue et al. 2010; Carrera et al. 2011; Georganopoulos et al. 2011; Melbourne et al. 2011; Rafferty et al. 2011; Mullaney et al. 2012a; Johnson et al. 2013; Wang et al. 2013a; Delvecchio et al. 2015; Rodighiero et al. 2015); (ii) far-IR/(sub-)mm followup observations of the star formation process in galaxies hosting X-ray selected AGNs (e.g., Page et al. 2004, 2012; Stevens et al. 2005; Lutz et al. 2010; Shao et al. 2010; Mainieri et al. 2011; Harrison et al. 2012, 2016; Mullaney et al. 2012b, 2015; Rosario et al. 2012; Rovilos et al. 2012; Santini et al. 2012b; Azadi et al. 2015; Barger et al. 2015; Stanley et al. 2015) or mid-IR/optically selected quasars (e.g., Omont et al. 1996, 2001, 2003; Carilli et al. 2001; Priddey et al. 2003; Wang et al. 2008b; Walter et al. 2009; Serjeant et al. 2010; Bonfield et al. 2011; Mor et al. 2012; Xu et al. 2015; Harris et al. 2016; Netzer et al. 2016).

These observational studies have revealed a well defined behavior of the average SFR in the host galaxies with respect to the AGN luminosity (see the review by Alexander & Hickox 2012); specifically, the SFR is found to be roughly constant for moderate AGN luminosities, while for high luminosities it stays constant or decreases in X-ray selected AGNs, and increases steeply in mid-IR or optically selected QSOs. A correlation between the average AGN luminosity and the stellar mass emerges also when focusing on mass-selected galaxy samples. All these relationships are often interchangeably referred to as “AGN main sequence.”

The theoretical interpretation, especially in the range of AGN luminosities investigated via X-ray stacking, is far from trivial; phenomenological models (Aird et al. 2013; Caplar et al. 2015; Hickox et al. 2014; Stanley et al. 2015) call into play AGN variability, as inspired from the merging scenario (see Di Matteo et al. 2005; Hopkins et al. 2005, 2013, 2016; Hopkins & Hernquist 2009; Novak et al. 2011) and inferred from consistency with the locally observed Eddington ratio distribution. Variability can effectively weaken an underlying correlation between AGN luminosity and SFR, if the AGN luminosity substantially changes (i.e., by more than an order of magnitude) over much shorter timescales than the star formation across the galaxy.

Here we aim at following a different, model-independent approach based on deterministic star formation and BH accretion histories, to provide a unifying physical interpretation on the origin, shape, scatter, and cosmic evolution for the main sequence of both star-forming galaxies and AGNs at high redshift $z \gtrsim 1$. To this purpose, we exploit: (i) the redshift-dependent SFR functions, based on the latest UV/far-IR data from HST/Herschel, and related statistics of strong gravitationally lensed sources; (ii) evolutionary tracks for the history of star formation and BH accretion, consistent with a wealth of multiwavelength observations including the observed Eddington ratio distribution at various $z$. We further validate these ingredients by showing their consistency with the observed stellar mass function of active galaxies, and with the AGN bolometric luminosity functions at different redshifts.

The plan of the paper is as follows: in Section 2 we deal with the main sequence of star-forming galaxies, exploiting the SFR
functions and deterministic star formation histories to physically interpret their shape, scatter, and cosmic evolution; in Section 3 we follow the same route to interpret the AGN main sequence, exploiting a deterministic BH accretion history consistent with a wealth of multiwavelength observations, and the AGN luminosity functions derived from our SFR functions; in Section 4 we summarize and critically discuss our findings.

In the present paper we adopt the flat cosmology indicated by the Planck Collaboration XIII (2016) data, with round parameters: Hubble constant $H_0 = 100\, h\, \text{km s}^{-1} \text{Mpc}^{-1}$ for $h = 0.67$, matter density $\Omega_M = 0.32$, baryon density $\Omega_b = 0.05$, and mass variance $\sigma_8 = 0.83$ on a scale of $8\, h^{-1}\, \text{Mpc}$. Galaxy stellar masses and luminosities (or SFRs) refer to Chabrier’s (2003) initial mass function (IMF).

2. THE MAIN SEQUENCE OF STAR-FORMING GALAXIES

Our analysis relies on two basic ingredients: a model-independent determination of the SFR functions at different redshifts, and the time dependence of the SFR within high-redshift star-forming galaxies, as inferred from observations and supported by simple physical arguments. We now describe these two ingredients in some detail, and then investigate the implications for the main sequence of star-forming galaxies.

2.1. SFR Functions

Our starting point is the global SFR function $dN/d\log M_\star$, namely the number density of galaxies per logarithmic bin of SFR [$\log M_\star$, $\log M_\star + d\log M_\star$] at given redshift $z$. This has been accurately determined on the basis of the most recent far-IR and UV data by Mancuso et al. (2016). We defer the interested reader to that paper for a detailed description of the procedure and of the extensive validation against independent data sets; here we recall some basic notions to be used in the following.

The SFR function has been built up by exploiting the most recent determinations of the luminosity functions at different redshifts from far-IR and UV data, with the latter being dust-corrected according to the $\beta_{\text{UV}}$–IRX relation (see Meurer et al. 1999; Calzetti et al. 2000; Bouwens et al. 2009, 2015, 2016). Specifically, in Mancuso et al. (2016), see their Figures 1 and 2 and Table 1) we adopted a Meurer/Calzetti extinction law, while in the present paper we switch to a Small Magellanic Cloud (SMC) extinction law that better describes the IR excess of UV-selected galaxies at $z \gtrsim 2$ (see Bouwens et al. 2016), especially at low SFR $M_\star \sim$ a few $10^9\, M_\odot\, \text{yr}^{-1}$. We note that the determination of the SFR functions is only marginally affected by the difference between the SMC and the Meurer/Calzetti extinction laws. The luminosity $L_{\text{SFR}}$ is converted into the SFR $M_\star$ using $\log M_\star/M_\odot\, \text{yr}^{-1} \approx -9.8 + \log L_{\text{SFR}}/L_\odot$, a good approximation both for far-IR and (intrinsically) UV luminosities under the assumption of a Chabrier IMF (see Kennicutt & Evans 2012).

Then a widely used, smooth analytic representation of the SFR function is found in terms of a standard Schechter shape

$$\frac{dN}{d\log M_\star}(M_\star, z) = N(z) \left[ \frac{M_\star}{M_\star(z)} \right]^{-\alpha(z)} e^{-M_\star/M_\star(z)}; \quad (1)$$

the redshift evolution for any parameter $p(z)$ of the Schechter function, i.e., the normalization $N$, the characteristic SFR $M_\star(z)$, and the faint end slope $\alpha$, has been described as a third-order polynomial in log-redshift $p(z) = p_0 + p_1\, z + p_2\, z^2 + p_3\, z^3$ with $z = \log(1 + z)$. The values of the evolution parameters $\{p_i\}$ have been set by performing an educated fit to the data. Specifically, for redshift $z \lesssim 3$ UV data are fitted for SFRs $M_\star \lesssim 30\, M_\odot\, \text{yr}^{-1}$ since in this range dust corrections based on the $\beta_{\text{UV}}$–IRX ratio are reliable, while far-IR data are fitted for SFRs $M_\star \lesssim 10^2\, M_\odot\, \text{yr}^{-1}$ since in this range dust emission is largely dominated by molecular clouds and reflects the ongoing SFR. On the other hand, for $z \gtrsim 8$ the (dust-corrected) UV data are considered reliable estimators of the intrinsic SFR function, since the amount of dust in a star-forming galaxy is expected to be rather small for an age of the universe shorter than $6 \times 10^9$ years. With these anchor points, we interpolate the behavior of the SFR function at intermediate redshifts $z \sim 4$–8, where sampling by far-IR surveys is absent due to sensitivity limits of current instruments. The values of the fitting parameters are reported in Table 1 and the resulting SFR function for three representative redshifts $z \approx 1, 3,$ and 6 is illustrated in Figure 1.

All in all, at $z \gtrsim 4$ our estimate implies a significant number density of dusty star-forming galaxies with SFR $M_\star \gtrsim 10^2\, M_\odot\, \text{yr}^{-1}$, currently missed by UV data. To highlight more clearly this point, we also report in Figure 1 the SFR function that would have been inferred basing solely on UV data, dust corrected via the UV slope. These strongly underestimate the global SFR function for SFRs $M_\star \gtrsim 30\, M_\odot\, \text{yr}^{-1}$. This is because violent SFRs occur within heavily dust-shrouded molecular clouds, while the UV slope mainly reflects the emission from stars obscured by the diffuse, cirrus dust component (see Silva et al. 1998; Coppin et al. 2015; Reddy et al. 2015).

In Mancuso et al. (2016) we have validated the SFR functions against independent data sets, including galaxy number counts at signifcative submm/far-IR wavelengths, redshift distributions of gravitationally lensed galaxies, and cosmic infrared background. In Figure 2 we also illustrate the cosmic SFR density, computed as

$$\rho_{M_\star}(z) = \int d\log M_\star \frac{dN}{d\log M_\star} M_\star; \quad (2)$$

integrated as usual down to $0.03\, M_\odot\, \text{yr}^{-1}$ for fair comparison with data. The UV-far-IR result compares well with the observational estimate by Hopkins & Beacom (2006) based on multiwavelength data including radio. The UV-inferred result is appreciably lower especially at $z \lesssim 6$, and agrees better with the estimate by Madau & Dickinson (2014) mainly based on UV data dust corrected via the UV slope.

2.2. Star Formation History

We now focus on the star formation history $M_\star(\tau|M_\star, t)$; this quantity represents the behavior of the SFR $M_\star$ as a function of the internal galactic age $\tau$ (i.e., the time since the beginning of significant star formation) for a galaxy with stellar mass $M_\star$ at cosmological time $t$ (corresponding to redshift $z$). We base this on the indications emerging from many studies of SED-modeling for high $z \gtrsim 2$ star-forming galaxies (e.g., Papovich et al. 2011; Smit et al. 2012; Moustakas et al. 2013;
### Table 1
SFR Function Parameters

| Parameter | Far-IR+UV | UV (Dust-corrected) |
|-----------|----------|---------------------|
|           | $p_0$ | $p_1$ | $p_2$ | $p_3$ | $p_0$ | $p_1$ | $p_2$ | $p_3$ |
| $\log N(z)$ | $-2.53 \pm 0.06$ | $-5.81 \pm 1.19$ | $10.41 \pm 3.57$ | $-5.95 \pm 2.59$ | $-1.90 \pm 0.08$ | $-1.50 \pm 1.72$ | $4.28 \pm 4.46$ | $-5.41 \pm 3.02$ |
| $\log M_{*,b}(z)$ | $1.28 \pm 0.05$ | $4.71 \pm 0.62$ | $-1.67 \pm 1.70$ | $-3.3 \pm 1.21$ | $-0.04 \pm 0.05$ | $1.96 \pm 0.99$ | $1.87 \pm 2.55$ | $-2.48 \pm 1.72$ |
| $\alpha(z)$ | $1.29 \pm 0.01$ | $2.82 \pm 0.23$ | $-6.18 \pm 0.67$ | $4.20 \pm 0.46$ | $1.09 \pm 0.03$ | $3.39 \pm 0.61$ | $-7.53 \pm 1.60$ | $5.41 \pm 1.07$ |

**Note.** Quoted uncertainties are at 1-$\sigma$ level. Fits hold in the range of $SFR = 10^{-1} - 10^{2} M\odot$ yr$^{-1}$ and for redshifts $z \approx 0$–8. Here we adopt an SMC extinction law (for a Meurer/Calzetti law, see Table 1 in Mancuso et al. 2016).

Steinhardt et al. 2014; Cassará et al. 2016; Citro et al. 2016); these suggest a slow power-law increase of the SFR $M_*$, over a timescale $\tau_b$, followed by an exponential decline with timescale $\tau_{5\%}$: in the literature a similar time evolution is sometimes referred to as the “delayed exponential model” (see Lee et al. 2009). Such an overall behavior can be described as follows

$$M_*(\tau|\tau_b, t) = M_{*,b} \left( \frac{\tau}{\tau_b} \right)^{\alpha} \quad 0 \leq \tau \leq \tau_b$$

$$= M_{*,b} e^{-{(\tau - \tau_b)}/\tau_{5\%}} \quad \tau \geq \tau_b$$

with $\kappa \approx 0.5$; the value of the SFR $M_{*,b}$ at $\tau_b$ is easily related to the final stellar mass $M_*$ by the relation $M_{*,b} = M_* \left( \tau_b / (\kappa + 1) + \tau_{5\%} \right)^{-1}$.

As to the parameters involved in the above expressions, recent observations by ALMA have shown that in massive, high-redshift galaxies the star formation occurred over timescales $\tau_b \lesssim 0.5$–1 Gyr at violent rates $M_* \gtrsim 10^2$ $M\odot$ yr$^{-1}$ in heavily dust-shrouded environments (e.g., Scoville et al. 2014, 2016).

A duration of the main star formation episode $\tau_b \lesssim 0.5$–1 Gyr in massive high-redshift galaxies, which are thought to be the progenitors of local ellipticals, is indeed confirmed by observations of the $\alpha$-enhancement, i.e., iron underabundance compared to $\alpha$ elements. This occurs because star formation is stopped, presumably by AGN feedback, before SN Ia explosions can pollute the interstellar medium with substantial iron amounts (e.g., Thomas et al. 2005; Gallazzi et al. 2006 for a review see Renzini 2006). Contrariwise, in low-mass galaxies with $M_* \lesssim 10^{10} M\odot$ data on the age of stellar population and on chemical abundances indicate that star formation has proceeded for longer times, regulated by SN II feedback and galactic fountains (see the reviews by Conroy 2013 and Courteau et al. 2014).

On this basis, following Aversa et al. (2015) we parameterize the timescale for the duration of the main star formation episode as

$$\tau_b = 1 \text{ Gyr} \left( \frac{1 + z}{3.5} \right)^{-3/2} \left[ 1 + 2 \text{ erf} \left( \frac{4}{3} \log \left( \frac{M_*}{5 M\odot \text{yr}^{-1}} \right) \right) \right]$$

The dependence on cosmic time matches that of the dynamical time $t_c \propto 1/\sqrt{G \rho} \propto (1 + z)^{-3/2}$, in turn following the increase in average density $\rho \propto (1 + z)^{3}$ of the ambient medium.
Figure 3. Evolution with galactic age (in units of BH e-folding time $\tau_{\nu}$) of the luminosity (top panel) and mass (bottom panel), normalized at the time $\tau_{\nu}$ when the AGN luminosity peaks and the star formation is quenched by the AGN feedback. Solid lines refer to AGN-related quantities and dashed lines to star formation-related quantities. The orange area sketches the stage when the AGN X-ray forming galaxy is dust-enshrouded and appears as a far-IR bright source; the red area sketches the stage when the AGN luminosity peaks and the star formation is quenched by the AGN feedback. Solid lines refer to AGN-related quantities and dashed lines to star formation-related quantities. The orange area sketches the stage when the AGN X-ray forming galaxy is dust-enshrouded and appears as a far-IR bright source; the red area sketches the stage when the AGN luminosity peaks and the star formation is quenched by the AGN feedback.

Figure 4. The stellar mass function of star-forming galaxies at $z = 2$ (red), 4 (orange), 6 (cyan), and 8 (blue) as derived from the SFR functions (see Figure 1) and from the star formation timescale $\tau_{\nu}$ (see Equation (4)) via the continuity equation (see Equation (5)). Solid lines refer to the global (UV+far-IR) SFR functions with a scatter $\sigma = 0.15$ dex in the star formation timescale $\tau_{\nu}$, the dashed line (only at $z = 2$ for clarity) refers to zero scatter, and dotted lines to the (dust-corrected) UV-inferred SFR functions. Data are from Aversa et al. (2015) and Mancuso et al. (2016). In Figure 4 we compare the resulting stellar mass function to the recent observational data at various redshifts, finding an excellent agreement.

As to the quenching timescale $\tau_{\nu}$, the observed fraction of far-IR-detected host galaxies in X-ray (e.g., Mullane et al. 2012b; Page et al. 2012; Rosario et al. 2012) and optically selected AGNs (e.g., Mor et al. 2012; Wang et al. 2013b; Willott et al. 2015) points toward an SFR abruptly stopping, at least in massive galaxies, after $\tau_{\nu}$ over a short timescale $\tau_{\nu} \lesssim 10^8$ years due to the action of AGN feedback.

In Figure 3 we show the ensuing star formation and BH accretion histories as a function of the galactic age. We test the adopted star formation history and timescales by connecting the SFR functions to the stellar mass function via the continuity equation. In the absence of merging terms, the continuity equation can be written as

$$\frac{dN}{d \log M_*}(M_*, t) = \int d \log M_* \partial_t \left[ \frac{dN}{d \log M_*}(M_*, t) \right]$$

$$\times \frac{d\tau}{d \log M_*}(M_*, t);$$

here the term on the lhs is the (known) SFR function, while under the integral on the rhs the first term is the cosmic time derivative of the (unknown) stellar mass function, and the second is the time spent by a galaxy in a bin of SFR obtained from the star formation history after Equation (3). We solve the continuity equation to derive the stellar mass function along the lines discussed by Aversa et al. (2015) and Mancuso et al. (2016).

2.3. Interpreting the Galaxy Main Sequence

Given the ingredients above, we populate the SFR versus $M_*$ diagram as follows. The number of galaxies per logarithmic
In this respect, our outcome compares well with the observational determinations based on the statistics of large multiwavelength (UV+far-IR), mass-selected samples (white shaded areas) by Rodighiero et al. (2011, 2014) and by Speagle et al. (2014).

We remark that the main sequence originates naturally in our approach as a statistical locus in the SFR versus \( M_* \) plane. However, this by no means implies that an individual galaxy climbs along the main sequence during its lifetime. Typical evolutionary tracks followed by individual objects, as inspired by the in situ coevolution scenario (see Section 2.2), are illustrated by dotted lines; their shape is dictated by the slowly increasing SFR \( \dot{M}_* \propto \tau^{1/2} \) and appreciably rising stellar mass \( M_* \propto \tau^{3/2} \), which imply \( \dot{M}_* \propto M_*^{3/2} \). Then the main sequence with its associated variance corresponds to the portions of such tracks where galaxies spend most of their lifetime in logarithmic bins of \( M_* \), see Equation (7).

To highlight the relevance of observational selections different from that based on stellar mass, in Figure 5 we also report data points for individual, far-IR-selected galaxies by Koperski et al. (2016), Ma et al. (2015b), Negrello et al. (2014), along with Dye et al. (2015), and da Cunha et al. (2015) mainly at redshifts \( 1 \lesssim z \lesssim 3 \). We note that the observations by Koperski et al. are drawn from a SCUBA2 survey area of \( 10^5 \text{deg}^2 \); as a consequence, the former sample can probe galaxies with SFRs of few \( 10^2 \text{M}_\odot \text{yr}^{-1} \) at most, while the latter samples can probe galaxies with more extreme SFR values up to few \( 10^3 \text{M}_\odot \text{yr}^{-1} \), whose number density is substantially lower. On the other hand, all these far-IR samples are limited by instrumental sensitivity to a minimum SFR around \( 10^2 \text{M}_\odot \text{yr}^{-1} \). We also report data from the recent ALMA observations of the Hubble Ultra Deep Field over 4.5 arcmin\(^2\) by Dunlop et al. (2016).

It is remarkable that an appreciable fraction of the individual, far-IR selected galaxies lie above the main sequence, i.e., at SFR values higher than expected on the basis of the average relationship at given \( M_* \). A common interpretation of these off-main-sequence objects is that they are undergoing an episode of starburst triggered by a stochastic merger event. Although these instances may well occur especially at low redshift \( z \lesssim 1 \), our interpretation for the bulk of the objects at higher redshift \( z \gtrsim 1 \) differs substantially. On the basis of the evolutionary track of individual galaxies, we envisage off-main-sequence objects to be caught in an early evolutionary stage, and still accumulating their stellar mass. Since the SFR changes slowly during the evolution, far-IR selection is unbiased with respect to the stellar mass; thus young star-forming galaxies are found to be preferentially located above the main sequence or, better, to the left of it. As time goes by and stellar mass increases, the galaxy moves toward the average main sequence relationship, around which it will spend most of its lifetime. Afterwards, the SFR either slowly decreases because of gas exhaustion for galaxies with small final stellar mass, or is abruptly quenched by AGN feedback for galaxies with high final stellar mass. In particular, in the latter case the galaxy will then evolve passively to become a local early-type and will populate a region of the SFR versus \( M_* \) diagram substantially below the main sequence. These loci of “red and dead” galaxies are indeed observed locally (see Renzini & Peng 2015), and start to be pinpointed even at high redshift (see Man et al. 2016).
Figure 6. The main sequence of star-forming galaxies at $z \approx 2$, based on the global (UV+far-IR) SFR functions. The solid line with error bars illustrates the mean relationships with its 2σ scatter. The dotted lines show three evolutionary tracks (forward time direction indicated by arrows) for galaxies with a given final stellar mass of about $10^{10.5}; 10^{11.5}; 10^{12.5} M_\odot$. The dashed lines show the timescale $M_i/M_\odot = 10^{5.5}; 10^{6.5}; 10^{7.5}$, and $10^{8.5}$ years as labeled. Filled symbols (error bars omitted for clarity) refer to far-IR data for individual objects by Ma et al. (2015b; pentagons) and Da Cunha et al. (2015; stars), color-coded according to the SED-inferred age $\tau_{\text{age}}$ in bins $\tau_{\text{age}} \leq 10^5$ (blue), $10^5 \leq \tau_{\text{age}} \leq 10^5.5$ (cyan), $10^5.5 \leq \tau_{\text{age}} \leq 10^6$ (orange), and $\tau_{\text{age}} \geq 10^6$ (red). Data points for galaxies at $1 \leq z \leq 3$ are highlighted by a black contour.

Support for such an evolutionary picture comes from the estimates of the galaxy ages inferred from multicolor SED modeling by da Cunha et al. (2015) and Ma et al. (2015b). In Figure 6 we report the data points from the latter authors, with the galaxy age highlighted in different colors. It can be seen that galaxies at $z \approx 2$ (data points with black contours) located above the main sequence are preferentially younger and less massive, with ages substantially below a few $10^8$ year; those more distant from the main sequence locus feature smaller and smaller ages.

In Figure 7 we highlight that exploiting in Equation (6) the UV-inferred SFR functions (dust corrected via the UV slope) originate a main sequence diagram in strong disagreement with the observations at high SFRs and/or stellar masses, because the SFR and stellar mass functions are considerably undersampled in the UV, especially at the high-SFR/stellar mass end.

A more quantitative look at the number density of the main sequence outliers is presented in Figure 8, where we show the distribution of specific SFR, i.e., $sSFR = M_\star/M_i$; this is obtained by slicing the main sequence diagram for different stellar mass bins (color-coded). The outcome based on the global (UV+far-IR) SFR functions (solid lines) is in remarkably good agreement with the observed distributions from Ilbert et al. (2015; see also Rodighiero et al. 2011; Schreiber et al. 2015); the latter is a 24 μm selected sample extracted from the COSMOS and GOODS surveys, with robust SFR estimates via mid-/far-IR data from Spitzer/Herschel. On the other hand, the outcomes based on the UV-inferred SFR functions (dashed lines) substantially underpredict the observed number density of high SFR galaxies; this again reflects the undersampling of galaxies with high SFRs by the UV data.

A similar mismatch at high SFR occurs for the semianalytic model by Wang et al. (2008a), reported in Figure 8 (dotted-dashed lines) for the same stellar mass bins of the data. We also show the region (cyan shaded area) encompassed by the three recent merger-driven models considered in Guo et al. (2016). These refined models (see also Ciambur et al. 2013; Lamastra et al. 2013; Mitchell et al. 2014; Henriques et al. 2015; Schaye et al. 2015; Lacey et al. 2016), featuring both a quiescent and a starburst mode of star formation triggered by galaxy mergers, perform better than the Wang et al. model for stellar masses $M_i \leq 10^{10.5} M_\odot$, though still underpredicting somewhat the observed sSFR distribution at high sSFR. All in all, this comparison between merger-driven models and observations indicates that the merger-induced SFRs are too low and/or the duty cycles of the star formation episodes are too short (see also Fontanot et al. 2012; Brennan et al. 2016).

In Figure 9 we confront the outcome of our computation for the average main sequence of star-forming galaxies at different redshifts $z \approx 1, 3,$ and 6 to the observational determinations by Speagle et al. (2014), finding good agreement. For comparison, the data points from individual observations presented in the previous figures are also reported, with their estimated redshift...
Figure 9. The main sequence of star-forming galaxies at $z \approx 1$ (red), 3 (green), and 6 (blue), based on the global (UV+far-IR) SFR functions. The solid lines with error bars illustrate the mean relationships with $2\sigma$ scatter. The dashed lines show the timescale $M_{\star}/M_\nu = 10^7$, $10^8$ and $10^9$ years as labeled. The shaded areas are the observational determinations of the main sequence at different redshifts (based on statistics of large samples) by Speagle et al. (2014). Filled symbols (error bars omitted for clarity) refer to far-IR data for individual objects by Dunlop et al. (2016; squares), Koprowski et al. (2016; diamonds), Ma et al. (2015b; pentagons), Negrello et al. (2014) plus Dye et al. (2015; circles), and Da Cunha et al. (2015; stars), color-coded according to redshift bins $z \lesssim 2$ (red), $2 \lesssim z \lesssim 4$ (green), and $z \gtrsim 4$ (blue).

highlighted in color. The observed redshift evolution of the main sequence is consistent with a scenario which traces the bulk of the star formation in galaxies back to local, in situ condensation processes. Specifically, at higher $z$ and in massive galaxies, the interstellar medium is on average denser $\rho \propto (1 + z)^3$; both the dynamical $t_d \propto 1/\sqrt{\rho} \propto (1 + z)^{-3/2}$ and the cooling $t_c \propto 1/\rho \propto (1 + z)^{-3}$ timescales become shorter, and the SFR $M_{\star} \propto M_{\star}/\max[t_d, t_c]$ associated with a galaxy of given stellar mass is higher, causing the main sequence locus to shift upwards. We stress that, moving toward higher redshift, the fraction of off-main-sequence objects decreases appreciably; this is because, given the evolution of the SFR function and the shorter age of the universe, it is more and more difficult to spot galaxies of appreciably different ages and featuring very high SFRs.

3. THE MAIN SEQUENCE OF AGNS

As discussed in Section 1, nowadays it has been widely established that the mass of central BHs in massive, early-type galaxies is intimately linked to several properties of the hosts (e.g., velocity dispersion, stellar mass, etc.). However, a hot debate is still open on the physical origin of this link, in particular concerning the interplay between the star formation and BH accretion processes. Many studies pointed out the existence of an AGN main sequence, which relates the AGN luminosity to the SFR and/or stellar mass of the host star-forming galaxy. We stress that the AGN main sequence is actually a coevolution plane, since it involves both AGN and host galaxy properties; as such it differs from the stellar main sequence, which relates only star-related variables.

In the following we discuss the BH accretion history as inferred from a wealth of multiwavelength observations. We show that it can be exploited to map the SFR functions into AGN bolometric luminosity functions, in excellent agreement with recent determinations. Then we turn to interpret and physically understand the AGN main sequence.

3.1. BH Accretion History

The BH accretion history in high-$z$ star-forming galaxies can be robustly constrained from a wealth of multivlavelength observations concerning: (i) the fraction of far-IR detected galaxies in X-ray selected AGNs (e.g., Mullaney et al. 2012b; Page et al. 2012; Rosario et al. 2012) and optically selected quasars (e.g., Mor et al. 2012; Wang et al. 2013b; Willott et al. 2015); (ii) the fraction of X-ray detected AGNs in far-IR/K-band selected host galaxies (e.g., Alexander et al. 2005; Mullaney et al. 2012a; Johnson et al. 2013; Wang et al. 2013a); (iii) stacking of undetected sources (e.g., Basu-Zych et al. 2013).

Lapi et al. (2014) and Aversa et al. (2015) have interpreted these data in terms of a very basic physical scenario of in situ coevolution. In a nutshell, this envisages that the early growth of the nuclear BH in high-redshift star-forming galaxies occurs under heavily dust-enshrouded conditions. In the early stages $\tau \ll \tau_{\bullet}$, plenty of gas is available from the surroundings, and the BH accretes at substantial, mildly super-Eddington rates $\lambda \gtrsim 1$, so as to develop radiatively inefficient slim-disk conditions (see Abramowicz et al. 1988; Watarai et al. 2000; Li 2012; Madau et al. 2014; Volonteri et al. 2015).

During these early stages the BH luminosity is substantially smaller than that of the star-forming host galaxy, that shines as a (sub)-mm bright source with an X-ray nucleus. After a time $\tau \approx \tau_{\bullet} \lesssim \text{Gyr}$, the nuclear power progressively increases to values similar to or even exceeding that of the host galaxy. Strong BH winds remove interstellar gas and dust while quenching star formation, so that the system behaves as an optical quasar. Residual gas present in the central regions of the galaxy can be accreted onto the BH at progressively lower, sub-Eddington accretion rates; the accretion disk becomes thin, yielding the standard SEDs observed in type-1 AGNs (Elvis et al. 1994; Hao et al. 2014). In quantitative terms, the typical AGN lightcurve can be described as (Yu & Lu 2004; Lapi et al. 2014; Aversa et al. 2015)

$$L_{\text{AGN}}(\tau|M_{\text{BH}}, \sigma) = L_{\text{AGN}, b} e^{(\tau-\tau_{\bullet})/\tau_e}$$

$$0 \leq \tau \leq \tau_{\bullet}$$

$$L_{\text{AGN}}(\tau|M_{\text{BH}}, \sigma) = L_{\text{AGN}, b} e^{-(\tau-\tau_{\bullet})/\tau_{\text{AGN}}} \tau \geq \tau_{\bullet}$$

(8)

During the early phase up to the time $\tau_{\bullet}$ the BH mass increases exponentially with characteristic timescale $\tau_e$ up to a value $M_{\text{BH}, e}$; the AGN emits with an Eddington ratio $\lambda \gtrsim 1$ until reaching a peak luminosity $L_{\text{AGN}, b} = \lambda M_{\text{BH}, e} c^2/\tau_{\text{Edd}}$. Then a late phase when the luminosity exponentially declines with a characteristic timescale $\tau_{\text{AGN}}$ follows. The quantities $\lambda$ and $\epsilon$ refer to the average radiative efficiency and Eddington ratio during the early phase, so that the $e$-folding time reads $\tau_{\text{e}} = \epsilon \tau_{\text{Edd}}/\lambda (1 - \epsilon)$. As to the characteristic time $\tau_{\text{AGN}}$ of the declining phase, the data on the fraction of star-forming host galaxies in optically selected quasars suggest a value $\tau_{\text{AGN}} \approx 3 \tau_e$ for AGNs with peak luminosities $L_{\text{AGN}, b} \gtrsim 10^{13} L_\odot$; on the other hand, AGNs with lower peak luminosity are constrained to fade more drastically after the peak (Lapi et al. 2014 and Aversa...
et al. 2015). These behaviors can be smoothly rendered as
\[
\tau_{\text{AGN}} = 3 \tau_{\text{et}} \left[ 1 - \frac{1}{2} \text{erfc} \left( \frac{1}{2} \log \frac{L_{\text{AGN},b}}{10^{43} L_{\odot}} \right) \right].
\] (9)

As to the Eddington ratio \( \lambda \), its evolution with redshift is strongly constrained by various observations, including the bright end of the optical AGN luminosity function, the observed Eddington ratio function (see Vestergaard & Osmer 2009; Kelly & Shen 2013; Schulze et al. 2015), and the fraction of AGN hosts with given stellar mass as a function of the Eddington ratio (see Aird et al. 2012; Bongiorno et al. 2012). The implied dependence of \( \lambda \) on \( z \) can be rendered approximately as (see Lapi et al. 2014; Aversa et al. 2015)
\[
\lambda(z) = 4 \left[ 1 - \frac{1}{2} \text{erfc} \left( \frac{z - 2}{3} \right) \right].
\] (10)

Note that during the early stages \( \lambda \gtrsim \lambda_{\text{thin}} \approx 0.3 \) holds and a radiatively inefficient slim accretion disc is expected (Laor & Netzer 1989); since the Eddington ratio lowers rapidly, a thin accretion disc develops during the late evolution.

As to the radiative efficiency \( \epsilon \), a simple prescription relates it and the Eddington ratio \( \lambda \) for slim/thin discs (see Abramowicz et al. 1988; Watari et al. 2000; Blandford & Begelman 2004; Li 2012; Madau et al. 2014) in the form
\[
\epsilon = \frac{\epsilon_{\text{thin}}}{2} \frac{\lambda}{\epsilon^{\lambda/\beta - 1}};
\] (11)

here \( \epsilon_{\text{thin}} \approx 0.57-0.32 \) refers to the efficiency during the thin disc phase, that depends on the BH spin (Thorne 1974). A fiducial value \( \epsilon_{\text{thin}} = 0.1 \) is suggested by statistical investigations based on the continuity equation (e.g., Cao 2010; Aversa et al. 2015) and from observations of individual systems (see Davis & Laor 2011; Raimundo et al. 2012; Wu et al. 2013). In the early stages when mildly super-Eddington accretion occurs with \( \lambda \gtrsim 0.3 \) \( \epsilon \approx \epsilon_{\text{thin}} \approx 0.03 \), while in the late stages when sub-Eddington accretion occurs, it quickly approaches the thin disc value \( \epsilon \approx \epsilon_{\text{thin}} \approx 0.1 \).

The final BH mass \( M_{\text{BH}} \) is simply written in terms of the peak mass \( M_{\text{BH},p} \) appearing in Equation (8) via \( L_{\text{AGN},b} \); it reads
\[
M_{\text{BH}} = \int_0^{\infty} d\tau \frac{1 - \epsilon}{e^{\epsilon/\beta}} L_{\text{AGN}}(\tau) = M_{\text{BH},p} \left[ 1 + f_{\epsilon} \frac{\tau_{\text{AGN}}}{\tau_{\text{et}}} \right].
\] (12)

The factor \( f_{\epsilon} \) takes into account the modest change of \( (1 - \epsilon)/\epsilon \) during the declining phase, when \( L_{\text{AGN}}(\tau) \) and \( \lambda(\tau) \) decrease almost exponentially and \( \epsilon(\tau) \) increases according to Equation (11); a value \( f_{\epsilon} \approx 0.8 \) corresponds to a good accuracy.

The evolution of the AGN luminosity and BH mass during the galaxy timetime \( \tau \) is illustrated in Figure 3.

3.2. Mapping the SFR Functions into the AGN Luminosity Functions

We stress that the above BH accretion history and timescales have not only been inferred from a plethora of observational data, but also have been validated in Aversa et al. (2015) by showing that the BH mass function obtained via the continuity equation approach well reproduces the current observational constraints at different redshifts (e.g., Shankar et al. 2009, 2013; Vika et al. 2009; Willott et al. 2010; Li et al. 2011; Ueda et al. 2014).

Here we provide a further validation, by examining the AGN statistics from a galaxy evolution viewpoint, basing on the SFR functions and on a deterministic BH accretion history consistent with the Eddington ratio distribution at various redshifts (see Figures 8 and 9 in Aversa et al. 2015). This is similar in spirit with, but different operationally from, the approach by Caplar et al. (2015), who recovered the AGN luminosity functions from the stellar mass functions and from an ad hoc Eddington ratio distribution.

To relate the BH accretion and star formation histories, we set the final BH/stellar mass ratio \( M_{\text{BH}}/M_* \), to average values \( \approx 10^{-3} \) with a scatter \( \approx 0.4 \) dex, as directly measured in the local universe (see Shankar et al. 2016). Direct observational determinations and statistical estimates based on the abundance matching between the stellar and BH mass functions out to \( z \approx 2 \) indicate model-independently, though with large uncertainties, that the \( M_{\text{BH}}/M_* \) ratio weakly increases with redshift (e.g., Häring & Rix 2004; Peng 2007; Jahnke & Macciò 2011; Kormendy & Ho 2013; Aversa et al. 2015; Shankar et al. 2016). We render this average evolutionary behavior as
\[
\frac{M_{\text{BH}}}{M_*} = 1.5 \times 10^{-3} \left( 1 + \frac{z}{2} \right)^{\zeta},
\] (13)

with a fiducial value \( \zeta \approx 1/2 \), and assume a scatter of 0.4 dex independent of redshift around this mean relationship. We checked that our results on the AGN luminosity functions and AGN main sequence are marginally affected by varying \( \zeta \) in the plausible range from 0 to 1; note that a decrease in \( \zeta \) is easily offset by a moderate increase in the scatter toward high redshift, and vice versa.

The relative time spent by the AGN in a given logarithmic bin of luminosity \( L_{\text{AGN}} \), i.e., the AGN duty cycle, just reads
\[
\frac{d\delta}{d \log L_{\text{AGN}}} = \frac{\tau_{\text{et}} + \tau_{\text{AGN}}}{\tau_{\text{et}} + \xi \tau_{\text{AGN}}} \ln 10;
\] (14)

here the total duration of the AGN luminous phase is taken as \( \tau_{\text{et}} + \xi \tau_{\text{AGN}} \) with \( \xi \approx 3 \), since after that time the luminosity has already decreased by a factor \( e^{-\xi} \approx 0.05 \) and the BH mass has already attained its final value to a very good approximation; in any case, variations of this parameter do not appreciably affect our results.

Then the AGN bolometric luminosity function can be straightforwardly computed as
\[
\frac{dN}{d \log L_{\text{AGN}}} = \int d \log M_* \frac{dN}{d \log M_*} \frac{d\delta}{d \log L_{\text{AGN}}}. \] (15)

The outcome is illustrated in Figure 10 at various redshifts, and pleasingly agrees with the most recent observational determinations. This further validates the proposed BH accretion history.

Basing on the UV-inferred SFR functions would clearly undersample the AGN luminosity functions at the bright end, since the number of galaxies with high SFR and high stellar mass, hence with high BH mass and AGN luminosity, is itself underestimated. Note that, as shown by the dotted lines in Figure 1, AGNs with appreciable X-ray luminosity \( L_X \gtrsim 10^{42} \) erg s\(^{-1}\) (bolometric corrections by Hopkins...
The scatter. The variance when adopting, for a fair comparison with data, a stochastic variability model by Hickox et al. (2014) and Stanley et al. (2015), inspired by the merger-driven scenario (see Equations (18) and (19)). Optical data (filled symbols) are from Richards et al. (2006; circles), Fan et al. (2006; pentagons), Croom et al. (2009; crosses), Jiang et al. (2009; inverse triangles), Willott et al. (2010; pacmans), Masters et al. (2012; triangles), Ross et al. (2013; stars), and Palanque-Delabrouille et al. (2016; diamonds). X-ray data (empty symbols) are from Fiore et al. (2012; spirals), Ueda et al. (2014; squares), Aird et al. (2015; big cross), and Miyaji et al. (2015; hexagons). The X-ray and optical luminosities have been converted to bolometric by using the corrections from Hopkins et al. (2007; see their Figure 1), while the number densities have been corrected for obscured AGNs following Ueda et al. (2003, 2014).

et al. 2007 have been adopted) are hosted by galaxies with SFRs $M_{SFR} \gtrsim 100 M_\odot$ yr$^{-1}$, but their number density is smaller than that of the overall star-forming population by a factor $\lesssim 10^{-4}$; this is because of the duty cycle (see Equation (14)), which reflects the nearly constant behavior of the SFR versus the exponential growth of the BH accretion rate during the galaxy lifetime.

In Figure 2 we report the cosmological evolution of the BH accretion rate density, computed as

$$\rho_{\text{BH}} = \int d\log L_{\text{AGN}} \frac{dN}{d\log L_{\text{AGN}}} \frac{L_{\text{AGN}}}{c^3}$$

(16)

with a reference value $\epsilon \approx 0.1$ of the radiative efficiency. We show the results for two minimum values of $L_{\text{BH}} \gtrsim 10^{42}$ and $10^{43}$ erg s$^{-1}$, to cope with the observational limits in the estimate of the luminosity functions at $z \lesssim 3$ and $z \gtrsim 3$, respectively. Our combined results compare well with the observational estimates by Aird et al. (2015) from X-ray selection and by Delvecchio et al. (2014) from an IR perspective. It is interesting to note that the cosmic BH accretion rate and SFR densities feature a similar evolution, with a peak around $z \sim 2$–3 and a decline toward higher redshift. We stress that this is a statistical outcome originated by the shape of the SFR and AGN luminosity functions; by no means does it imply that within an individual galaxy the BH accretion rate is always proportional to the SFR.

The outcome at the representative redshift $z \approx 2$ is presented in Figure 10, which shows the AGN luminosity (right axis) vs. the bolometric luminosity (left axis) at $z \approx 2$, based on the global (UV+far-IR) SFR functions and the AGN duty cycle associated to the deterministic BH accretion history of Section 3.1. Colored contours illustrate the number density of galaxies plus AGNs (labels in log units of Mpc$^{-3}$). The solid line with error bars illustrates the mean relationship with its 2$\sigma$ scatter. The dashed line represents the locus where $L_{\text{SFR}} = L_{\text{AGN}}$. The dotted lines show three evolutionary tracks (forward time direction indicated by arrows) for objects with a given peak AGN luminosity of $10^{44.7}, 10^{45.1}, 10^{45.3}$ erg s$^{-1}$. The dotted–dashed line is the average relationship obtained by adopting the variability model by Hickox et al. (2014) and Stanley et al. (2015), inspired by the merger-driven scenario (see Equations (18) and (19)). Data are from: Page et al. (2012; pentagons) for both individual (filled symbols) and stacked (open symbols) X-ray selected sources; Stanley et al. (2015; circles) for stacked X-ray selected sources; Harrison et al. (2016; stars) for individual X-ray selected sources; Netzer et al. (2016; squares) for both individual and stacked optically selected sources; Xu et al. (2015; triangles) for individual mid-IR selected sources; Delvecchio et al. (2015; diamonds) for stacked far-IR selected sources.

### 3.3. Interpreting the AGN Main Sequence

Given consistent SFR functions, AGN duty cycles and luminosity functions, we can investigate the AGN main sequence. We start from discussing the $L_{\text{AGN}}$ versus SFR diagram. The number of objects per logarithmic bin of AGN luminosity and SFR is given by

$$\frac{dN}{d\log M_*, d\log L_{\text{AGN}}} \approx \frac{dN}{d\log M_*} \frac{d\delta}{d\log L_{\text{AGN}}}.$$ (17)

The outcome at the representative redshift $z \approx 2$ is presented in Figure 11, where the color-code indicates the logarithmic number density of objects per unit comoving volume in Mpc$^{-3}$). The solid line with errorbars illustrates the number density-weighted mean relationship ($M_*$) at given $L_{\text{AGN}}$ with its 2$\sigma$ variance when adopting, for a fair comparison with data, a SFR detection limit of $10^{-2} M_\odot$ yr$^{-1}$. Our deterministic evolutionary tracks for the star formation and corresponding BH accretion history in individual galaxies (dotted lines), and the locus where the AGN and SFR luminosities match (dashed line), are also illustrated.

For AGN luminosities $L_{\text{AGN}} < L_{\text{SFR}}$ lower than those associated with star formation, the tracks of individual objects and the mean relationships are flat; in fact, this occurs for galactic ages $\tau \lesssim \tau_{\text{gb}}$ when the SFR is roughly constant while the AGN luminosity grows exponentially. Then on moving toward higher AGN luminosities $L_{\text{AGN}} \gtrsim L_{\text{SFR}}$, the AGN gets rapidly suppressed and the AGN luminosity fades, so that the evolutionary tracks of individual objects move toward the bottom left region of the
diagram. Contrariwise, the mean relationship starts to increase, being statistically dominated by objects with higher and higher SFR; this is because to achieve a higher AGN luminosity, the BH must reside in a galaxy with larger SFR.

In the diagram we illustrate, for comparison, data points from individual and stacked observations of X-ray selected AGNs (Page et al. 2012; Stanley et al. 2015; Harrison et al. 2016), mid-IR selected AGNs (Xu et al. 2015), and optically selected quasars (Netzer et al. 2016). The position on the diagram of these data points can be easily understood as a selection effect (see Figure 3). Optical selection tends to pick up objects close to the peak of AGN luminosity when, in the host, dust has been partially removed and the SFR starts to be quenched; X-ray selection can pick up objects before or after the AGN peak, hence with SFR in the host still sustained or suppressed, respectively. Mid-IR selection with the current observational limits strikes an intermediate course between the former two.

For the sake of completeness, we also report data for a sample of far-IR selected galaxies, where the bolometric AGN luminosity has been estimated by stacking of X-ray fluxes (Delvecchio et al. 2015). In each of the SFR bins, the nuclear luminosity spans a range of values, because the galaxy can be picked up at any time before the peak, when the AGN luminosity can have vastly different values. Note that the contour levels reported in the figure apply if the primary selection is in AGN luminosity, and not in far-IR emission associated with star formation in the host.

In Figure 11 the average result based on the variability model by Hickox et al. (2014) and Stanley et al. (2015) is also shown. These authors adopt an Eddington ratio (or AGN luminosity) distribution inspired by merger-driven models of galaxy formation, that translates into a duty cycle with shape

\[
\frac{d\delta}{d \log L_{\text{AGN}}} \propto \left( \frac{L_{\text{AGN}}}{100 \langle L_{\text{AGN}} \rangle} \right)^{-\omega} e^{-L_{\text{AGN}}/100 \langle L_{\text{AGN}} \rangle},
\]

where \( \omega \approx 0.2 \) (actually Hickox et al. 2014 adopt \( \omega \approx 0.6 \), but the results change little); the distribution is normalized to unity over the range \( L_{\text{AGN}} > 10^{-2} \langle L_{\text{AGN}} \rangle \).

The above authors also assume a constant ratio \( M_{BH}/M_* \approx 1/3000 \) between the BH accretion rate and the SFR, as observed in the local universe (e.g., Chen et al. 2013); this provides a link between SFR and average AGN luminosity \( \langle L_{\text{AGN}} \rangle \) in the form

\[
\langle L_{\text{AGN}} \rangle \approx 2 \times 10^{42} \text{ erg s}^{-1} \times \frac{M_*}{M_S} \text{ yr}^{-1}.
\]

Such a stochastic model produces a result (lilac dot-dashed line) similar to ours (lilac solid line) on the SFR versus \( L_{\text{AGN}} \) diagram. However, as shown from Figure 10 it considerably underpredicts the observed bolometric AGN luminosity functions at \( z \geq 1 \), especially at the bright end. This is because Equation (19) implies a too low normalization of the SFR to the BH accretion rate (1/3000) at high redshift, and Equation (18) is not sufficiently broad at the bright end (see Bongiorno et al. 2012; Nobuta et al. 2012; Kelly & Shen 2013).

We now turn to interpret the diagram \( L_X \) (or \( L_{\text{AGN}} \)) versus \( M_* \). The number of objects per logarithmic bin of AGN luminosity and stellar mass is given by

\[
\frac{d^2N}{d \log M_* d \log L_{\text{AGN}}} \approx \int d \log M_* \frac{dN}{d \log M_*} \frac{d\delta}{d \log L_{\text{AGN}}} \frac{d\delta}{d \log M_*},
\]

where the relative times spent by a galaxy with approximately constant SFR in a bin of AGN luminosity and stellar mass are given in Equations (14) and (7). The outcome at the representative redshift \( z \approx 2 \) is presented in Figure 12, where the color-code indicates the logarithmic number density of objects per unit comoving volume (in Mpc\(^{-3}\)). The lilac line with error bars illustrates the relationship averaged over detected and stacked sources (dashed lines) with its 2\( \sigma \) variance, for a detection limit at \( L_X \approx 10^{46} \text{ erg s}^{-1} \). The dotted lines show three evolutionary tracks (forward time direction indicated by arrows) for objects with a given peak AGN luminosity of \( 10^{46} \), \( 10^{45.5} \), \( 10^{45} \text{ erg s}^{-1} \). Data are from Delvecchio et al. (2015); squares for far-IR selected sources, from Mullaney et al. (2015b); diamonds for X-ray-selected sources; and from Mullaney et al. (2012a); stars and Rodighiero et al. (2015; circles) for mass-selected samples; the open circles illustrate the average for detected (top) and stacked (bottom) sources in the Rodighiero et al. (2015) data.

The evolutionary tracks for individual galaxies (dotted lines) feature a spiky behavior. This is because, as can be inferred from Figure 3, both during the ascending and the declining part of the AGN lightcurve, the AGN luminosity increases or decreases exponentially, while the stellar mass varies little; e.g., before the AGN luminosity peak, the behavior \( M_* \propto \sqrt{\log L_{\text{AGN}}} \) applies after Equations (3) and (8). This absence of correlation between \( L_{\text{AGN}} \) and \( M_* \) is consistent with the observations of X-ray-selected AGNs by Mullaney et al. (2012b); as mentioned above, X-ray selection tends to pick up objects both before and after the AGN peak, when the AGN luminosity can be vastly different while the stellar mass changes little.

The mean relationship for detected galaxies (upper lilac dashed line) increases with stellar mass; this is because to achieve a high AGN luminosity, the BH must reside in a galaxy with rather high stellar mass, due to the constraint on the BH-
to-stellar mass ratio at the end of the coevolution, that is pinpointed by a mass-selected sample (see Equation (13)). This well agrees with the average relationship for X-ray detected AGNs in the mass-selected galaxy sample by Rodighiero et al. (2015 upper empty circles).

However, the mean relationship when including stacked observations (Mullaney et al. 2015; Rodighiero et al. 2015) lies substantially below, because of the contribution of undetected sources to the average. To compare with these data, it is essential to account for the contribution from star formation to the X-ray emission. In our computation we estimate the X-ray luminosity from star formation by the calibration

$$L_{X,SFR} = 7 \times 10^{39} \text{erg s}^{-1} \times \frac{M_*}{M_\odot \text{yr}^{-1}}$$

(21)

of Vattakunnel et al. (2012).

We stress that the X-ray emission from star formation is usually negligible in individual detected sources with X-ray luminosity $L_X \gtrsim 10^{42} \text{erg s}^{-1}$, corresponding for standard bolometric corrections to $L_{LUM,AGN} \gtrsim 10^{44} \text{erg s}^{-1}$. Contrariwise, when stacking sources with detection threshold $L_X \lesssim 10^{42} \text{erg s}^{-1}$, the galaxy number density can be largely dominated by star-forming galaxies with negligible nuclear activity. As a consequence, the relation for undetected sources could just mirror the galaxy main sequence, with SFR converted in X-ray luminosity after Equation (21). We find this is indeed the case, with the resulting average relationship for undetected sources (lower lilac dashed line) being a factor about $10^2$ below that for detected AGNs, in agreement with Rodighiero et al. (2015; lower empty circles). We caution that, for such undetected sources, the conversion in bolometric luminosity via the standard X-ray correction for AGNs is somewhat misleading.

The average over detected and stacked sources (lilac solid line) strikes an intermediate course, and is found to be in excellent agreement with the observational determinations by Mullaney et al. (2015) and Rodighiero et al. (2015); however, its straight physical interpretation is hampered because the statistics of detected and undetected objects is contributed by different processes, i.e., either BH accretion or star formation, respectively.

In Figure 13 we show the average ratio between the X-ray luminosity (or BH accretion rate) and the SFR versus the stellar mass. Note that for a fair comparison with observational data by Mullaney et al. (2015) and Rodighiero et al. (2015), the BH accretion rate has been obtained from the X-ray luminosity by converting to bolometric with the standard X-ray correction for AGNs and then using $\dot{M}_{BH} = (1 - \epsilon)L_{AGN}/c^2$ with $\epsilon \approx 0.1$. The result is another representation of the previous diagram, so our computation is again based on Equation (17), and the same cautionary comments apply. Specifically, detected sources are truly AGNs, while the undetected sources are mainly main sequence galaxies with negligible nuclear activity. The average relationship $L_X/M_* \propto M_*^{0.5}$ weakly increases with the stellar mass, in agreement with the latest data from Rodighiero et al. (2015).

We stress that such a behavior of the average relationship (mean of detected plus stacked sources) between X-ray luminosity (or BH accretion rate, strictly holding only for detected sources) and the SFR does not mean that the quantities are proportional during the galaxy lifetime. In fact, the evolutionary tracks for individual objects are characterized by a very steep trend; this is because, during the ascending phase, the AGN luminosity increases exponentially, while the SFR is roughly constant and the stellar mass increases mildly with time. It is only in a statistical sense that the weakly increasing behavior with $M_*$ emerges.

Finally, we note that the normalization of the average ratio around a few $10^{-4}$ at $M_* \approx 10^{11}M_\odot$ is driven by the statistics of stacked sources, which is mainly contributed by star-forming galaxies with negligible nuclear activity. In fact, the relationship for detected X-ray AGNs lies a factor around 10 above, with normalization increased to a few $10^{-3}$ at $M_* \approx 10^{11}M_\odot$; indeed this reflects the value of the BH to stellar mass ratio at the end of the coevolution, as pinpointed by a mass selection.

4. SUMMARY AND CONCLUSIONS

We have provided a novel, unifying physical interpretation on the origin, average shape, scatter, and cosmic evolution for the main sequences of star-forming galaxies and AGNs at high redshift $z \gtrsim 1$. We have achieved this goal in a model-independent way by exploiting: (i) the redshift-dependent SFR functions by Mancuso et al. (2016), based on the latest UV and far-IR data from HST, Herschel, and validated on several grounds; (ii) deterministic evolutionary tracks for the history of star formation and black hole accretion, gauged on a wealth of multiwavelength observations. We further validate these ingredients by showing their consistency with the observed galaxy stellar mass functions and AGN bolometric luminosity functions at different redshifts via the continuity equation approach.

Our main findings are as follows:

1. The galaxy main sequence and its scatter originate naturally as a statistical relationship from the SFR functions and a deterministic star formation history. The existence of the main sequence by no means implies that individual galaxies evolve along it. Specifically, we
envisage young objects to be preferentially located to the left of the main sequence at given SFR. As the time goes by they will move at nearly constant SFR toward the main sequence locus, spending most of their lifetime there. Afterwards, their SFR will be reduced and the galaxy will move below the main sequence, occupying the locus of “red and dead” objects, as observed locally. Such a picture provides strong support for an in situ scenario for star formation in galaxies.

2. Off-main sequence galaxies are interpreted as young objects, that have still to accumulate most of their stellar mass. In this respect, the interpretation of their peculiar position in the SFR versus \( M_* \) diagram is not to be above the main sequence at given stellar mass, but rather to be to the left of it at a given SFR. Mass-selected galaxies tend to preferentially lie on the main sequence, while far-IR selected ones are unbiasedly picked up on it or to the left of it. The age estimates via SED modeling of far-IR selected galaxies support our interpretation, showing a tendency for objects more distant from the main sequence locus to feature smaller and smaller ages. Note that this is in contrast to the interpretation of off-main-sequence objects as starbursts triggered by mergers or cosmological inflows.

3. We are also able to explain the redshift evolution of the main sequence toward higher SFRs at given stellar mass, tracing star formation in galaxies back to in situ condensation processes. At higher \( z \) these are typically more efficient, yielding more violent SFRs, and so causing the main sequence locus to shift upwards. We also expect that, going toward higher redshift, the number of off-main-sequence objects decreases appreciably.

4. The AGN main sequence is globally understood in terms of star formation and BH accretion histories. As to the SFR versus \( L_{\text{AGN}} \) relationship, we expect a flat behavior for AGN luminosities lower than those associated with star formation, reflecting the individual evolutionary tracks of young galaxies. Then on moving toward higher AGN luminosities, the SFR gets rapidly suppressed by feedback processes, and the AGN luminosity itself slowly fades, so that the evolutionary tracks of individual objects move toward the bottom left region of the diagram. Contrariwise, the mean SFR increases with AGN luminosity, being statistically dominated by more massive objects that feature higher and higher SFRs.

5. As to the \( L_X \) versus \( M_* \) relationship, we expect that the evolutionary tracks for individual galaxies feature a spiky behavior, because the AGN luminosity increases or decreases exponentially with the galactic age, while the stellar mass varies little. This absence of correlation is consistent with the observations of X-ray selected AGNs. On the other hand, the mean \( L_X \) for detected galaxies increases almost linearly with \( M_* \), being statistically dominated by objects with higher stellar and BH masses. The resulting relation agrees well with the average relationship for X-ray detected AGNs in mass-selected galaxy samples. However, when including stacked observations the mean \( L_X \) is substantially lower, because of the contribution of undetected sources. We have highlighted that the statistics of undetected sources is dominated by star-forming galaxies with negligible AGN emission, and so it reflects the galaxy main sequence, with SFR converted in X-ray luminosity. As such, a straight physical interpretation of the mean relationship is hampered because the statistics of detected and undetected objects is contributed by different processes, i.e., either BH accretion or star formation, respectively.

6. Finally, we have discussed the increase of the average ratio between BH accretion rate and the SFR as a function of galaxy stellar mass. This does not imply that the BH accretion rate and SFR are proportional during the entire galaxy lifetime, because the average relationship holds only for detected sources in a statistical sense.

The star formation and BH accretion histories emerging from the above observational landscape constitute a testbed for galaxy and AGN evolution models; in particular, they provide a guide to gauge recipes in semianalytic models and subgrid physics in numerical simulations.

We have shown that to properly interpret the main sequences for star-forming galaxies and AGNs at high redshift \( z \gtrsim 2 \) future observations should aim at: (i) exploiting different selections for galaxies and AGNs to fully populate the main sequence diagrams, especially for detected sources; (ii) measuring with improved accuracy the ages of stellar populations for extended samples of star-forming galaxies and AGN hosts; (iii) determining via spectroscopic observations the gas content of star-forming galaxies and AGN hosts located on and above the main sequences. To study off-main sequence objects, an important issue concerns the stellar mass determination of far-IR selected galaxies at high-redshift, that will become feasible in the near future thanks to the James Webb Space Telescope.

In the present paper we have provided a unified view on galaxy and supermassive BH evolution. In fact, while there is a large consensus on BH evolution via in situ accretion processes, debate is still open on the role of mergers or cosmological gas inflows in the assembly of stellar mass within galaxies. All in all, our analysis of the main sequence for high-redshift galaxies and AGNs highlights that the present data can be consistently interpreted in terms of an in situ coevolution scenario, that strongly demands to be further tested via future observations.

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