Data Article

Thermodynamic and thermoelastic data of georesources raw minerals: Zinc sulphide and apatite

Gianfranco Ulian, Giovanni Valdrè*
Dipartimento di Scienze Biologiche, Geologiche e Ambientali, Centro di Ricerche Interdisciplinari di Biomineralogia, Cristallografia e Biomateriali, Università di Bologna “Alma Mater Studiorum” Piazza di Porta San Donato 1, 40126 Bologna, Italy

ARTICLE INFO

Article history:
Received 28 January 2020
Received in revised form 30 January 2020
Accepted 3 February 2020
Available online 8 February 2020

Keywords:
Raw mineral georesources
Zinc sulphide
Apatites
Zinc sulphide polymorphs
Type-A carbonated apatite
Thermodynamic and thermoelastic properties
DFT
Quasi-harmonic approximation

ABSTRACT

This article reports a dataset on the thermodynamic and elastic properties of two important raw minerals exploited in georesources and ore mining. The presented data refers to two zinc sulphide polymorphs, namely zinc-blende (low-pressure polymorph, space group $F_43m$) and rock-salt (high-pressure polymorph, space group $Fm3m$) [1], and of type-A carbonated apatite, [Ca$_{10}$PO$_4$]$_3$CO$_3$, space group $P1$] [2]. The data here reported were calculated from ab initio quantum mechanical simulations at the DFT/B3LYP level, all-electron Gaussian-type orbitals basis sets and from the analysis of the phonon properties of the zinc sulphide polymorphs and of type-A CAp by means of the quasi-harmonic approximation. In addition, a correction to take into account the effects of dispersive forces was considered to obtain the dataset of type-A carbonated apatite. This dataset, which was validated against experimental thermodynamic data reported in literature, has been employed to construct the phase diagram between the two zinc sulphide polymorphs and discuss their stability over the temperature and pressure range 0–800 K and 0–25 GPa. The thermodynamic and thermoelastic data of CAp were obtained between 0 and 600 K and 0–3 GPa, below the temperature of thermal decomposition of the mineral. The reported data can be of use in several application fields, for instance fundamental georesource exploration and exploitation, and also in applied mineralogy, geology, material science, and as a reference to assess the quality of other theoretical approaches. Furthermore, the data...
of type-A carbonated apatite could be useful for designing and processing new biomaterials with tailored properties.

© 2020 The Authors. Published by Elsevier Inc. This is an open access article under the CC BY-NC-ND license (http://creativecommons.org/licenses/by-nc-nd/4.0/).

Specifications Table

| Subject                      | Material Science                                           |
|------------------------------|------------------------------------------------------------|
| Specific subject area        | Thermodynamics and thermoelastic of georesources raw minerals |
| Type of data                 | Table, Graph, Figure                                       |
| How data were acquired       | Quantum mechanical simulations at the DFT/B3LYP level of theory, using the quasi-harmonic approximation (CRYSTAL17 code) |
| Data format                  | Raw, Analyzed                                              |
| Parameters for data collection | The temperature and pressure range used in the quasi-harmonic approximation for the calculation of the thermodynamic and thermoelastic data were 0–800 K (step of 1 K) and 0–25 GPa (step of 1 GPa) for zinc sulphides and were 0–600 K (step of 1 K) and 0–3 GPa (step of 1 GPa) for type-A carbonated apatite |
| Description of data collection | The data were obtained from quantum mechanical simulations conducted using Density Functional Theory, B3LYP functional and Gaussian-type orbitals basis sets. A correction for the dispersive forces based on the DFT-D2 method was also employed (B3LYP-D* scheme) for type-A carbonated apatite. The quasi-harmonic approximation, based on the volume dependence of mineral phonon properties at different temperatures and hydrostatic compression states, was employed to calculate the thermodynamic and thermoelastic dataset. Starting geometries used as input for the quantum mechanical simulations were taken from experimental structural results. |
| Data source location         | The quantum mechanical simulations were conducted at the University of Bologna, Bologna, Italy. |
| Data accessibility           | With the article                                           |
| Related research articles    | Ulian, G. & Valdrè, G. (2019) Thermomechanical, electronic and thermodynamic properties of ZnS cubic polymorphs: an ab initio investigation on the zinc-blende — rock-salt phase transition. Acta Crystallographica Section B, 75, 1042–1059, doi:https://doi.org/10.1107/S2052520619012630. |
|                             | Ulian, G., and Valdrè, G. (2019) First principle investigation of the thermomechanical properties of type A carbonated apatite. International Journal of Quantum Chemistry, 120, e26069, https://doi.org/10.1002/qua.26069. |

Value of the Data

- A detailed dataset on thermodynamic and thermoelastic properties of zinc sulphide polymorphs (zinc-blende and rock-salt ZnS) and of type-A carbonated apatite \([\text{Ca}_{10}(\text{PO}_4)_6\text{CO}_3]\) represents a foundation for future fundamental and applied studies on these mineral phases.
- Both theoretical and experimental researchers could employ this dataset as a valuable reference to compare the results of their studies.
- This dataset provides also fundamental insights on the zinc-blende and rock-salt ZnS phases, which could be employed, for example, to devise pressure/temperature sensors.
- In addition, being zinc sulphide an ore mineral, this dataset could be employed for development of ore mineral processing techniques.
- Carbonated (hydroxy)apatite is a key biomaterial for bone reconstruction and repair, and the provided data can drive future researches and developments in the biomaterial field.
1. Data description

1.1. Zinc sulphide polymorphs: zinc-blende and rock-salt ZnS

Zinc-blende (zb, also known as sphalerite from the mineralogical point of view) and rock-salt ZnS (rs) are two polymorphs of zinc sulphide, belonging to the space group $F\overline{4}3m$ and $Fm\overline{3}m$, respectively. Zb-ZnS is stable at low pressure and temperatures, representing the main source of zinc from ore smelting, whereas rs-ZnS is found at high pressures. Sphalerite is found in several locations worldwide, such as Germany, Romania, Canada, USA and Mexico. To realize the present dataset, both polymorphs were optimized at equilibrium conditions and under the effect of hydrostatic expansion/compression at $T = 0$ K, starting from the experimental structures determined by Skinner [3]. The unit cell geometry optimization results for both zb-ZnS and rs-ZnS are reported in Table 1 [1], whereas Fig. 1 shows a graphical representation of the unit cell energy vs volume curves fitted by a volume-integrated 3rd-order Birch-Murnaghan equation of state.

The thermodynamics and thermomechanics of both zb-ZnS and rs-ZnS were calculated from the phonon properties of the mineral phases between 0 and 800 K. The effect of pressure was evaluated from 0 GPa to 20 GPa for zinc-blende, whereas for the rock-salt polymorph, which presents phonon instability at low pressure [1], the properties were calculated in the pressure range 12–25 GPa. The results are reported in Tables S1–S22 in the Supplementary Material for both zb-ZnS (Tables S1–S11) and rs-ZnS (Tables S12–S22), subdivided as follows:

- primitive unit cell volume (Tables S1 and S12);
- isothermal bulk modulus, $K_T$ (Tables S2 and S13);
- adiabatic bulk modulus, $K_S$ (Tables S3 and S14);
- coefficient of thermal expansion (CTE), $\alpha_V$ (Tables S4 and S15);
- isochoric heat capacity, $C_V$ (Tables S5 and S16);
- isobaric heat capacity, $C_P$ (Tables S6 and S17);
- entropy, $S$ (Tables S7 and S18);
- absolute enthalpy, $H$ (Tables S8 and S19);
- absolute Helmholtz free energy, $F$ (Tables S9 and S20);
- absolute Gibbs free energy, $G$ (Tables S10 and S21);
- absolute internal energy, $U$ (Tables S11 and S22).

The obtained reported data can be employed, for instance, to create bidimensional plots of the desired thermodynamic and thermoelastic properties and to compare them to other theoretical or experimental results. Fig. 2 reports an example of this application.

### Table 1

Primitive unit cell volume ($V_{pc}$) and static energy ($E_{pc}$), Crystallographic unit cell volume ($V_{cc}$) and lattice parameter ($a_{pc}$) resulting from the geometry optimization results of zinc-blende and rock-salt ZnS polymorphs. Underlined values are related to the equilibrium geometry.

| Zinc-blende ZnS | Rock-salt ZnS |
|----------------|--------------|
| $P$ (Gpa) | $V_{pc}$ ($A^3$) | $E_{pc}$ (Ha) | $V_{cc}$ ($A^3$) | $a_{cc}$ ($A$) | $P$ (Gpa) | $V_{pc}$ ($A^3$) | $E_{pc}$ (Ha) | $V_{cc}$ ($A^3$) | $a_{cc}$ ($A$) |
| 21.30 | 35.080 | $-2.177214945324E+03$ | 140.321 | 5.197 | 25.65 | 29.042 | $-2.177192422262E+03$ | 116.170 | 4.879 |
| 16.23 | 36.377 | 145.506 | 5.260 | 19.48 | 30.116 | $-2.177197962616E+03$ | 120.462 | 4.939 |
| 11.81 | 37.704 | $-2.177224760714E+03$ | 150.818 | 5.323 | 14.14 | 31.215 | $-2.177202180969E+03$ | 124.860 | 4.998 |
| 7.95 | 39.064 | 156.257 | 5.386 | 9.51 | 32.341 | $-2.177205213821E+03$ | 129.362 | 5.058 |
| 4.59 | 40.456 | $-2.177229880849E+03$ | 161.825 | 5.449 | 5.51 | 33.493 | $-2.177207182795E+03$ | 133.972 | 5.117 |
| 1.67 | 41.881 | $-2.177230818510E+03$ | 167.524 | 5.513 | 2.07 | 34.672 | $-2.177208195666E+03$ | 138.691 | 5.176 |
| 0.05 | 42.781 | $-2.177230994348E+03$ | 171.123 | 5.552 | 0.18 | 35.418 | $-2.177208358995E+03$ | 141.670 | 5.213 |
| -0.87 | 43.339 | $-2.177230942467E+03$ | 173.355 | 5.576 | -0.90 | 35.880 | $-2.177208348407E+03$ | 143.518 | 5.236 |
| -3.06 | 44.830 | $-2.177230262299E+03$ | 179.320 | 5.639 | -3.44 | 37.114 | $-2.177207726602E+03$ | 148.457 | 5.295 |
| -4.95 | 46.355 | $-2.177228851914E+03$ | 185.421 | 5.702 | -5.61 | 38.377 | $-2.177206406104E+03$ | 153.507 | 5.354 |
| -6.57 | 47.915 | $-2.177226778287E+03$ | 191.658 | 5.766 | -7.46 | 39.668 | $-2.177204454375E+03$ | 158.671 | 5.414 |
1.2. Type-A carbonated apatite

Type-A carbonated apatite [Ca\(_{10}\)(PO\(_4\))\(_6\)CO\(_3\), space group \(P1\)] belongs to the calcium apatite mineralogical family, which is used for several applications, such as production of fertilizers, gemstone cutting and as source of rare-Earth elements through ore smelting. Carbonated apatite is also an important mineral in the biomaterials field. Apatite minerals are commonly found in Canada, Brazil, USA and Mexico.

Fig. 1. Primitive unit-cell volume vs energy data (reported as \(\Delta E = E - E_{\text{eq}}\) with \(E_{\text{eq}}\) equal to the energy of the unit cell at equilibrium volume) of (a) zinc-blende and (b) rock-salt ZnS. The box reports the parameters obtained from fitting the data with a volume-integrated 3rd-order Birch-Murnaghan equation of state.

Fig. 2. Bidimensional contour plots of (a,b) isobaric heat capacity and (c,d) primitive cell volume as a function of temperature and pressure for (a,c) zb-ZnS and (b,d) rs-ZnS.
The thermodynamic and thermoelastic data here provided were calculated from the structural and vibrational properties of seven unit cell volumes in the temperature range 0–600 K (step of 1 K), below the temperature of thermal decomposition of the mineral phase [4], and between 0 GPa and 3 GPa (step of 0.5 GPa). The equilibrium geometry was theoretically determined in a previous work [5], where the experimental results of Fleet and Liu [6] were employed to model the type-A carbonated apatite. The results are reported in Tables S23–S33 in the Supplementary Material whose content is here summarized:

- unit cell volume (Table S23);
- isothermal bulk modulus, $K^T$ (Table S24);
- adiabatic bulk modulus, $K^S$ (Table S25);
- coefficient of thermal expansion (CTE), $\alpha^V$ (Table S26);
- isochoric heat capacity, $C^V$ (Table S27);
- isobaric heat capacity, $C^P$ (Table S28);
- entropy, $S$ (Table S29);
- absolute enthalpy, $H$ (Table S30);
- absolute Helmholtz free energy, $F$ (Table S31);
- absolute Gibbs free energy, $G$ (Table S32);
- absolute internal energy, $U$ (Table S33).

2. Experimental design, materials, and methods

The data here presented was obtained by first principle simulations on periodic systems, using the CRYSTAL17 code [7], which implements the Hartree–Fock and Kohn–Sham self-consistent field method.

Multielectron wave functions are constructed as an antisymmetrized product (Slater determinant) of monoelectronic crystalline orbitals (CO) that are linear combination of local functions (atomic orbitals, AO) centred on each atom in the system. In turn, atomic orbitals (basis set) are linear combinations of Gaussian-type functions (GTF). The all-electron basis sets employed for both $\text{Zn}^{2+}$ and $S^2$ were described by the double-$\zeta$ basis set with polarization functions designed by Peintinger-Bredow-Oliveira (POB) [8]. For type-A CAp, it was the same basis sets adopted in previous works on OHAp and type A CAp [2,5]. Calcium has been described with an 86-511G(2d), with outer shell exponents $\alpha_{sp} = 0.453$ bohr$^{-2}$, $\alpha_{d1} = 3.1910$ and 0.8683 bohr$^{-2}$ and $\alpha_{d2} = 0.2891$ bohr$^{-2}$. The phosphorus atom is described by the basis 85-21G(d), $\alpha_{sp} = 0.48105$ bohr$^{-2}$ and $\alpha_d = 0.135$ and 0.74583 bohr$^{-2}$, respectively. Oxygen was represented by a 6-31G* basis set with the outer shell exponents $\alpha_{sp} = 0.2742$ and $\alpha_d = 0.190$ bohr$^{-2}$ and $\alpha_d = 0.538$ bohr$^{-2}$. The carbon atom is described by a 6-21G* basis set with $\alpha_{sp} = 0.26$ bohr$^{-2}$ and $\alpha_d = 0.8$ bohr$^{-2}$.

The hybrid B3LYP functional [9,10], which is well-known for its ability to produce high quality of crystal-chemical, vibrational/thermodynamic and elastic results [11,12], has been adopted for all calculations. Only in the case of type-A carbonated apatite, the DFT-D2 correction scheme was included in its recently adjusted form for B3LYP (B3LYP-D* approach) to take into account the effect of dispersive forces on both structural and thermodynamic properties [13]. The exchange–correlation contribution is performed over a grid of points and is the result of a numerical integration of the electron density and its gradient. The adopted pruned grid is given by 75 points and 974 angular points (XLGRID) and obtained from The Gauss–Legendre quadrature and Lebedev schemes. The tolerance thresholds that control accuracy of the Coulomb and exchange integrals were set to $10^{-7}$ and $10^{-16}$, respectively [7]. The Hamiltonian matrix has been diagonalized using a Monkhorst grid of k-points of size $8 \times 8 \times 8$ for both zinc-blende and rock-salt polymorphs. The convergence on total energy was reached when the difference between the energy of two subsequent self-consistent field cycles was less than $10^{-8}$ Hartree during geometry optimization and less than $10^{-10}$ Hartree during phonon calculations.

The compressional behaviour of zinc sulphide and type-A carbonated apatite has been investigated carrying out a symmetry-preserving relaxation procedure by exploring ten volumes between $0.82 \times V_{eq}$ and $1.12 \times V_{eq}$ (step of $0.03 \times V_{init}$) for both zinc-blende and rock-salt ZnS, whereas for type-A Cap seven
unit cell volumes were considered between 0.92×\(V\text{eq}\) and 1.08×\(V\text{eq}\), with a step of 0.04×\(V\text{eq}\) under compression (two unit cell volumes) and 0.02×\(V\text{eq}\) under expansion (four unit cell volumes). Here, \(V_{\text{init}}\) represents the volume of the unit cell of each mineral (zinc-blende, rock-salt ZnS, CAP) at equilibrium conditions. Each model was then geometrically optimized.

At each unit cell compressive state, the energy vs volume data, \(E(V)\) curve, was fitted with a volume-integrated 3rd-order Birch-Murnaghan equation of state (EoS) formulation [14]:

\[
E = E_0 + \frac{9}{16}K_0V_0\left(K'(\eta^2-1)^3 + \left(\left(\eta^2 - 1\right)\left(6 - 4\eta^2\right)\right)\right) \tag{1}
\]

\[
\eta = \left(\frac{V_0}{V}\right)^{1/3} \tag{2}
\]

where \(V_0\) is the unit cell volume at 0 GPa, \(E_0\) its energy, \(K_0\) the bulk modulus and \(K'\) the pressure first derivative of the bulk modulus. The obtained parameters were employed in the well-known \(P-V\) formulation of the Birch-Murnaghan EoS to calculate the pressure state of the system:

\[
P = \frac{3}{2}K_0\left[\eta^{-7/3} - \eta^{-5/3}\right] \left\{1 - \frac{3}{4} \left(4 - K\right)\left(\eta^{-2/3} - 1\right)\right\} + P_0 \tag{3}
\]

Thermodynamic and thermomechanics properties of each mineral phase were obtained from lattice dynamics results by means of the quasi-harmonic approximation (QHA) approach as described by Erba and co-workers [15]. Lattice dynamics was calculated on \(4 \times 4 \times 4\) supercells in the case of zinc sulphide polymorphs [1], whereas only \(\Gamma\)-point frequencies were considered for type-A carbonated apatite [2].

Acknowledgments

This research did not receive any specific grant from funding agencies in the public, commercial, or not-for-profit sectors.

Conflict of Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Appendix A. Supplementary data

Supplementary data to this article can be found online at https://doi.org/10.1016/j.dib.2020.105265.

References

[1] G. Ulian, G. Valdrè, Thermomechanical, electronic and thermodynamic properties of ZnS cubic polymorphs: an ab initio investigation on the zinc-blende – rock-salt phase transition, Acta Crystallogr. B 75 (2019) 1042–1059.
[2] G. Ulian, G. Valdrè, First principle investigation of the thermomechanical properties of type A carbonated apatite, Int. J. Quant. Chem. 120 (2019), e26069.
[3] B.J. Skinner, Unit-cell edges of natural and synthetic sphalerites, Am. Mineral. 46 (1967) 1399–1411.
[4] S.M. Barinov, J.V. Rau, S.N. Cesaro, J. Durišín, I.V. Fadeeva, D. Ferro, L. Medvecky, G. Trionfetti, Carbonate release from carbonated hydroxyapatite in the wide temperature range, J. Mater. Sci.: Mater. Med. 17 (2006) 597–604.
[5] G. Ulian, G. Valdrè, M. Corno, P. Ugliengo, Periodic ab initio bulk investigation of hydroxylapatite and type A carbonated apatite with both pseudopotential and all-electron basis sets for calcium atoms, Am. Mineral. 98 (2013) 410–416.
[6] M.E. Fleet, X.Y. Liu, Carbonate apatite type A synthesized at high pressure: new space group (P(3)over-bar) and orientation of channel carbonate ion, J. Solid State Chem. 174 (2003) 412–417.
[7] R. Dovesi, V.R. Saunders, C. Roetti, R. Orlando, C.M. Zicovich-Wilson, F. Pascale, B. Civalleri, K. Doll, N.M. Harrison, I.J. Bush, P. D’Arco, M. Llunell, M. Causì, Y. Noel, L. Maschio, A. Erba, M. Rerat, S. Casassa, CRYSTAL17 User’s Manual, University of Turin, Turin, 2017.
[8] M.F. Peintinger, D.V. Oliveira, T. Bredow, Consistent Gaussian basis sets of Triple-Zeta valence with polarization quality for solid-State Calculations, J. Comput. Chem. 34 (2013) 451–459.

[9] A.D. Becke, Density-functional thermochemistry. 3. The role of exact exchange, J. Chem. Phys. 98 (1993) 5648–5652.

[10] C.T. Lee, W.T. Yang, R.G. Parr, Development of the colle-salvetti correlation-energy formula into a functional of the electron-density, Phys. Rev. B 37 (1988) 785–789.

[11] G. Ulian, G. Valdrč, Effects of fluorine content on the elastic behavior of topaz Al2SiO4(F,OH)(2), Am. Mineral. 102 (2017) 347–356.

[12] G. Ulian, D. Moro, G. Valdrč, First principle investigation of the mechanical properties of natural layered nanocomposite: clinohlorite as a model system for heterodesmic structures, Compos. Struct. 202 (2018) 551–558.

[13] B. Civalleri, C.M. Zicovich-Wilson, L. Valenzano, P. Ugliengo, B3LYP augmented with an empirical dispersion term (B3LYP-D') as applied to molecular crystals, CrystEngComm 10 (2008) 405–410.

[14] M. Hebbache, M. Zemzem, Ab initio study of high-pressure behavior of a low compressibility metal and a hard material: osmium and diamond, Phys. Rev. B 70 (2004).

[15] A. Erba, J. Maul, R. Demichelis, R. Dovesi, Assessing thermochemical properties of materials through ab initio quantum-mechanical methods: the case of alpha-Al2O3, Phys. Chem. Chem. Phys. 17 (2015) 11670–11677.