Guaranteed Detection of a Minimal Supersymmetric Model 
Higgs Boson at Hadron Supercolliders

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Abstract

We demonstrate that expected efficiencies and purities for $b$-tagging at SSC/LHC detectors should allow detection of at least one of the Higgs bosons of the Minimal Supersymmetric Model in $t \bar{t}$ Higgs production, with Higgs $\rightarrow b \bar{b}$ decay, over a substantial range of supersymmetric parameter space. In particular, with the addition of this mode to those previously considered, there is no region of supersymmetric parameter space for which \textit{none} of the Higgs bosons of the model can be seen at the SSC/LHC.

1. Introduction and Procedure

Understanding the Higgs sector is a crucial mission for future high energy colliders such as the SSC and LHC. While it is quite certain that the SSC/LHC will be able to detect the Standard Model Higgs boson ($\phi^0$), prospects for detection of the Higgs bosons of the Minimal Supersymmetric Model (MSSM) have appeared to be somewhat limited. In particular, in previous work\textsuperscript{[1,2]} it became apparent that for $m_t \sim 150$ GeV there is a window of $m_{A^0}$-$\tan \beta$ parameter space, with $110 \lesssim m_{A^0} \lesssim 170$ GeV and $\tan \beta \gtrsim 10$, in which it could be that no MSSM Higgs boson would be seen either at LEP-II or at the SSC/LHC. (There is an even larger window where none could be seen just at the SSC/LHC.) For the former window to arise it is necessary that the squark mass be large enough ($\sim 1$ TeV) that radiative corrections\textsuperscript{[3]} to the mass of the lightest CP-even Higgs boson ($h^0$) are big, in particular, big enough that $Z^* \rightarrow Zh^0$ is not kinematically allowed at LEP-II when $\tan \beta$ is large and $m_{A^0}$ takes on moderate to large values. In addition, the presence of this window of unobservability is based on the assumption that only the $\gamma \gamma$ and $4\ell$ decay channels of the CP-even $h^0$ and $H^0$ Higgs bosons will lead to viable signals at the SSC/LHC,\textsuperscript{*} and that detection of the

\textsuperscript{*} Detection of the CP-odd $A^0$ in the $\gamma \gamma$ or $4\ell$ decay channels is confined to the region of parameter space where $\tan \beta \lesssim 1$. 
$H^{\pm}$ will be possible only if $t \to H^{\pm}b$ decays are kinematically allowed. Although it is not impossible that the portion of the window with very high $\tan \beta$ (where inclusive $b\bar{b}$ fusion yields enhanced Higgs boson cross sections) can be covered using the $\tau^{+}\tau^{-}$ decay modes of the $H^{0}$ and the $A^{0}$,[4] the precise parameter region over which it can be employed is a subject of continuing study.[5] In this letter, we demonstrate that a viable signal at the SSC/LHC for the primary decays $h^{0} \to b\bar{b}$ or $H^{0} \to b\bar{b}$ can be obtained in $t\bar{t}$ Higgs production over much of $m_{A^{0}}$–$\tan \beta$ parameter space (in particular, in the window in question).

In a previous paper,[6] we established that detection of the SM $\phi^{0}$ in the $t\bar{t}b\bar{b}$ final state mode was, indeed, possible for a significant range of $m_{\phi^{0}}$, provided $m_{t} \gtrsim 130 - 140$ GeV. The analysis of the present paper is based on the results of this previous work, to which we refer the reader for details. Several different detection scenarios were examined there. Here we consider only the case in which 3 $b$-quarks are required to be vertex tagged with efficiency of 30% and purity of 1% (after appropriate kinematic and vertex separation cuts). For this scenario, termed case I in Ref. 6, substantial peaks in the $\bar{b}b$ mass spectrum are visible for $\phi^{0}$ masses in the region below about 110 – 120 GeV. Of course, as argued in Ref. 6, it might be that the above assumptions regarding $b$-tagging efficiency and purity are too conservative. Detection of the MSSM Higgs bosons in the $t\bar{t}b\bar{b}$ final state mode would be even easier if, for instance, the $b$-tagging probability could be brought up to 40% while decreasing the misidentification probability to 0.5% over the stated kinematic range.

To convert the case I results for use in the MSSM, the following procedure is employed. First, we give the statistical significance of the $b\bar{b}$ mass peaks at Higgs masses of 80, 100, 120 and 140 GeV, for $m_{t} = 110, 140$ and 180 GeV, for $L = 10$ fb$^{-1}$ at the SSC assuming 100% $b\bar{b}$ branching ratio.[†] The number of standard deviations obtained for $m_{t} = (110, 140, 180)$ is (4.0,5.0,10.2), (3.2,3.4,6.5), (2.7,3.1,3.9) and (2.1,2.4,3.1) at Higgs masses of 80, 100, 120 and 140 GeV, respectively. Interpolation/extrapolation is employed to obtain results for the top quark masses of 150 GeV and 200 GeV considered here, and for other values of Higgs mass. The appropriate result for the $h^{0}$ or $H^{0}$ is obtained by multiplying the number of standard deviations by the $b\bar{b}$ branching ratio of the $h^{0}$ or $H^{0}$ and by the square of the ratio of the $h^{0}$ or $H^{0}$ $t\bar{t}$ coupling to the $\phi^{0}t\bar{t}$ coupling (to account for the difference in the $t\bar{t}$ Higgs production rates). Finally, if $t \to H^{\pm}b$ decays are allowed, the rate for the $t\bar{t}$ Higgs signal and for all the $t\bar{t}$-related backgrounds (see Ref. 6) must be appropriately reduced to account for the reduced trigger rate of an isolated lepton from one or two $t \to W^{\pm}b$ decays. Clearly, all these correction factors, not to mention the Higgs masses themselves, depend upon the supersymmetric model parameters, and in particular on $m_{A^{0}}$ and $\tan \beta$.

To understand the results we shall obtain, it is useful to review some features of the MSSM Higgs sector.[7] First, recall that the $h^{0}$ and $H^{0}$ mass eigenstates are obtained by diagonalizing the CP-even mass-squared matrix. The result for $\tan \beta \gtrsim 2$ is a kind of level-crossing in which for low $m_{A^{0}}$ the $H^{0}$ has a relatively constant mass value somewhat above $m_{Z}$. As $m_{A^{0}}$ increases, $m_{h^{0}}$ rises to ‘meet’ this constant value. For $m_{A^{0}}$ values above the crossing point, $m_{h^{0}}$ takes on a value which is a bit below or nearly the same (at large $\tan \beta$)

[†] Results for the LHC will not be given in this letter, but are substantially similar to those obtained for the SSC.
Figure 1: The ratios $g_{th}^2 / g_{t\phi_0}^2$ and $g_{bh}^2 / g_{b\phi_0}^2$ ($h = h^0, H^0$) are plotted as a function of $m_{A^0}$ at $\tan \beta = 2$ and $m_t = 150$ GeV. We have taken $M_{\tilde{t}} = 1$ TeV.

as the constant value while $m_{H^0}$ rises, becoming approximately degenerate with $m_{A^0}$. For $m_t \sim 150$ GeV and $M_{\tilde{t}} \sim 1$ TeV, the constant mass value referred to above is in the vicinity of 100 GeV, i.e. very much in the center of the mass region for which the $b\bar{b}$ mode $\phi^0$ studies were performed. For $m_t \sim 200$ GeV, the constant mass value is somewhat larger, in the vicinity of 130 GeV. The behavior of the $h^0$ and $H^0$ squared couplings to $b\bar{b}$ and $t\bar{t}$, relative to the $\phi^0$, as a function of $m_{A^0}$ is illustrated in Fig. 1. We see that at low $m_{A^0}$ the couplings of the $H^0$ are fairly SM-like, while after the crossing over (at $m_{A^0} \sim 100 - 130$ GeV) it is the $h^0$ which has SM-like couplings. Thus, whichever Higgs has mass in the vicinity of $m_Z$ (plus radiative corrections) is roughly SM-like.

However, the $b\bar{b}$ coupling for the Higgs with mass near $m_Z$ is not precisely the same as for the $\phi^0$. For $m_{A^0} \gtrsim 50$ GeV it is somewhat larger. This has the useful consequence that the $b\bar{b}$ branching ratios for the $H^0$ or $h^0$ can be nearer to 100% than for a $\phi^0$ of the same mass. Space does not allow a detailed exposition on the branching ratios of the $h^0$ and $H^0$. These are well-known.\cite{1,8} In general, $BR(h^0 \to b\bar{b})$ is very near 1 until $m_{\phi^0}$ becomes very close to its maximum value (at large $m_{A^0}$) at which point $BR(h^0 \to b\bar{b})$ declines somewhat as other modes enter the picture. The behavior of $BR(H^0 \to b\bar{b})$ as a function of $m_{A^0}$ is much more complicated and is highly dependent upon $\tan \beta$. In particular, $H^0 \to h^0 h^0$ severely suppresses the $H^0 \to b\bar{b}$ branching ratio for much of the relevant $m_{A^0}$ range when $m_{A^0} > 50$ GeV.\footnote{The precise number depends upon $\tan \beta$.}
tan $\beta$ is $\sim 2$. For larger $\tan \beta$, there is a window of moderate $m_{A^0}$ for which $BR(H^0 \to b\bar{b})$ is large. To illustrate, in Fig. 2 we plot $BR(h \to b\bar{b})$ as a function of $m_h$ ($h = h^0$ or $H^0$) for $m_t = 150$ GeV, and $\tan \beta = 2$ and 5.

2. Results and Discussion

Results for the SSC are displayed in Figs. 3 and 4, for $m_t = 150$ and 200 GeV, respectively. These figures display the regions of $m_{A^0}$-$\tan \beta$ parameter space where detection of $t\bar{t}h$ with $h \to b\bar{b}$ is possible at the 4$\sigma$ level for an integrated luminosity of $L = 30$ fb$^{-1}$ — the region of viability for $h = h^0$ is indicated by the letter i), while that for $h = H^0$ is indicated by h). The viable regions for an assortment of several other Higgs signals are also given in each case. The power of the $t\bar{t}b\bar{b}$ final state modes is immediately apparent.

In the case of $m_t = 150$ GeV, Fig. 3, the $h^0$ (i) and $H^0$ (h) $t\bar{t}b\bar{b}$ modes are viable in nearly all of parameter space above $m_{A^0} \sim 50$ GeV. The only exception is the delicate cross-over point discussed in the previous section of the paper, where the $H^0$ and $h^0$ switch roles. For $m_t = 150$ GeV the critical region is $m_{A^0} \sim 100-110$ GeV. For such $m_{A^0}$ values neither the $H^0$ nor the $h^0$ has full SM-strength $t\bar{t}$ coupling (see Fig. 1) and, strictly speaking, neither satisfies the 4$\sigma$ discovery criterion. However, it should be noted that for large $\tan \beta$ the $H^0$ and $h^0$ are nearly degenerate at the switch-over. Consequently, their mass peaks can be effectively lumped together, and the gap between the $H^0$ and $h^0$ regions is in reality not present for $\tan \beta \gtrsim 10$. The other curves given in Fig. 3 serve primarily to define the window (referred to in our introductory discussion), marked with a large $\times$, for which detection of a
Figure 3: Discovery contours (at the 4σ level) in $m_A$–tan $\beta$ parameter space for the SSC with $L = 30$ fb$^{-1}$ and LEP-200 with $L = 500$ pb$^{-1}$ for the reactions: a) $e^+e^- \rightarrow h^0Z$ at LEP-200; e) $W h^0X \rightarrow l\gamma\gamma X$; g) $t \rightarrow H^+b$; h) $t h^0$, with $H^0 \rightarrow b\bar{b}$; and i) $t h^0$, with $h^0 \rightarrow b\bar{b}$. The contour corresponding to a given reaction is labelled by the letter assigned to the reaction above. In each case, the letter appears on the side of the contour for which detection of the particular reaction is possible. The letter assignments are chosen to be consistent with those in J. Gunion and L. Orr, Ref. 1, and Refs. 2 and 9, in order to facilitate comparison with earlier results. The large $\times$ indicates the location of the window where no MSSM Higgs could be discovered at LEP-II or the SSC without processes h) and i). We have taken $m_t = 150$ GeV, $M_{\tilde{t}} = 1$ TeV and neglected squark mixing. Scenario (A) refers to the notation established in Ref. 9; it corresponds to the case in which charginos and neutralinos are taken to be heavy.
Figure 4: Discovery contours (at the 4σ level) in $m_A – \tan \beta$ parameter space for the SSC with $L = 30 \text{ fb}^{-1}$ and LEP-200 with $L = 500 \text{ pb}^{-1}$ for the reactions: a) $e^+e^- \rightarrow h^0Z$ at LEP-200; b) $e^+e^- \rightarrow h^0A^0$ at LEP-200; c) $h^0 \rightarrow 4l$; e) $W h^0X \rightarrow l\gamma X$; h) $t\bar{t}H^0$, with $H^0 \rightarrow b\bar{b}$; and i) $t\bar{t}h^0$, with $h^0 \rightarrow b\bar{b}$. Conventions as in Fig. 3, except that $m_t = 200 \text{ GeV}$.

MSSM Higgs boson at LEP-II or the SSC was previously deemed to be quite difficult. We see that the $t\bar{t}h^0$, $h^0 \rightarrow b\bar{b}$ mode is viable throughout this window region. In addition, we observe that if the LEP-II $Zh^0$ detection mode is removed, all but a tiny sliver of parameter
space is covered by the $t\bar{t}b\bar{b}$ mode of the $h^0$ or else by the $t \to H^+ b$ mode for $H^+$ detection. In addition, everywhere that $h^0$ detection in the $l\gamma\gamma$ final states (arising from $W h^0 X$ final states in which $W \to l\nu$ and $h^0 \to \gamma\gamma$) is possible, $h^0$ detection in the $t\bar{t}b\bar{b}$ final state is also possible.

At $m_t = 200$ GeV (Fig. 4), the $t\bar{t}b\bar{b}$ mode does not cover as large a fraction of parameter space. This is because the $h^0$ is substantially heavier when $m_{A^0}$ and $\tan \beta$ are both large ($m_{h^0} \gtrsim 130$ GeV), than in the $m_t = 150$ GeV case. Thus, $BR(h^0 \to b\bar{b})$ declines at large $m_{A^0}$ (see Fig. 2) due to the onset of $WW^*$ and $ZZ^*$ channels, while the $t\bar{t}h^0$ cross section is also somewhat smaller. However, there is no window of concern in this case; detection of at least one MSSM Higgs boson is possible throughout all of parameter space even without using the $t\bar{t}b\bar{b}$ modes. In Fig. 4, we have chosen to plot only those modes that allow detection of the $h^0$ (in particular, $t \to H^+ b$ and $H^0 \to 4\ell$ modes are not displayed) in addition to the $t\bar{t}b\bar{b}$ modes for the $h^0$ and $H^0$. This figure illustrates the substantial overlap among different $h^0$ detection modes. In particular, where modes c), e) and i) overlap, we should be able to experimentally verify the relative strengths of the $ZZh^0$, $t\bar{t}h^0$ and $b\bar{b}h^0$ couplings. In addition, we see that the $h^0$ can be discovered, either at LEP-II or the SSC for all but a window of parameter space with $\tan \beta \gtrsim 3.5$ and $70 \lesssim m_{A^0} \lesssim 150$ GeV.

For smaller values of $m_t$, e.g. in the vicinity of 100 GeV, the $t\bar{t}b\bar{b}$ detection mode for the $h^0$ remains viable over much the same region of parameter space as illustrated in Fig. 3 for $m_t = 150$ GeV. This is because radiative corrections to the $h^0$ mass are small, and the upper limit for $m_{h^0}$ (reached for $m_{A^0} \gtrsim 100$ GeV) lies between $\sim 50$ GeV and $m_Z$ for $\tan \beta$ between 2 and $\infty$. Thus, despite the increase of $t\bar{t}$-related backgrounds relative to those found for $m_t = 150$ GeV at any given Higgs mass, $m_{h^0}$ moves into a lower mass region where these backgrounds are actually smaller and the statistical significances (for 100% $b\bar{b}$ branching ratio) quoted earlier are larger. The region of viability for the $H^0$, whose mass remains in the vicinity of $m_Z$ for $m_{A^0} \lesssim 100$ GeV, does decrease somewhat at $m_t = 100$ GeV relative to $m_t = 150$ GeV because of the increased $t\bar{t}$-related background levels. Further details will be given in a longer paper.\textsuperscript{[0]} Of course, current indications from both the Tevatron and LEP are that $m_t$ is very likely to be $\gtrsim 130-140$ GeV. If $m_t$ were to turn out to be near 100 GeV, the $h^0$ mass is sufficiently small that LEP-II will have an excellent chance of detecting it in any case.

For $L = 100$ fb$^{-1}$, the LHC is roughly equivalent to the SSC at $L = 30$ fb$^{-1}$, assuming the same efficiency and purity of $b$-tagging. However, the efficiency of $b$-tagging at the LHC, given the many overlapping events expected, may not be as great as assumed here. Other experimental problems could arise regarding overlapping jets.

In the above, we have ignored the CP-odd $A^0$. This is because for both $m_t = 150$ and 200 GeV (and for $\tan \beta \gtrsim 0.5$) detection of the $A^0$ in the $t\bar{t}b\bar{b}$ mode is confined to a small area with $\tan \beta \lesssim 2$ and $m_{A^0}$ below roughly 130 GeV. The upper limit is given by the onset of the $A^0 \to Zh^0$ decay mode. Exactly how low we can go in $m_{A^0}$ at low tan $\beta$ values is not currently known. We estimate that the results of Ref. 6 can be safely extrapolated down to 50-60 GeV. But extension below that would require more detailed study. The inability to detect the $A^0$ for $\tan \beta \gtrsim 2$ is simply a consequence of the fact that the $A^0$$t\bar{t}$ coupling is
suppressed by $1/\tan\beta$. Thus, by $\tan\beta = 2$ the $A^0 t\bar{t}$ cross section is at most $1/4$ of SM size.\footnote{Actually, the $\gamma_5$ coupling also makes the cross section shape different as a function of Higgs mass, so that this scaling argument is not precise.}

Of course, in this letter we have focused on the case where supersymmetric partner masses are assumed to be large. The results for the $t\bar{t}b\bar{b}$ discovery modes of the $h^0$ and $H^0$ are essentially unmodified unless the chargino and/or neutralino masses lie below 50-60 GeV. This is because the $t\bar{t}b\bar{b}$ mode is mainly viable for regions of parameter space such that the Higgs ($h^0$ or $H^0$) mass is of order 80-130 GeV. If the squark mass is also taken to be light, then the region of viability for the $t\bar{t}b\bar{b}$ mode at $m_t = 200$ GeV actually expands since the $h^0$ has mass $\lesssim m_Z$, and thus will have nearly 100\% branching ratio to $b\bar{b}$, as well as being in the mass region of maximal sensitivity for the $t\bar{t}b\bar{b}$ mode. Of course, other SM final state detection modes do suffer if neutralinos and/or charginos are light. As detailed in Ref. 9, the $H^0 \to 4\ell$ mode is especially vulnerable. The power of the $t\bar{t}b\bar{b}$ detection modes, however, is such that the SSC alone remains able to see at least one MSSM Higgs boson throughout essentially all of MSSM parameter space.

3. Conclusion

We have demonstrated that $b$-tagging can be used to isolate $t\bar{t}h$ events, in which $h \to b\bar{b}$, for $h = h^0$ or $H^0$ over a substantial range of the parameter space of the Minimal Supersymmetric Model. With inclusion of this detection mode, for an accumulated luminosity of $L = 30$ fb$^{-1}$ the SSC alone is guaranteed to find at least one (and more probably several) of the MSSM Higgs bosons, for any value of $m_t \gtrsim 140$ GeV.

4. Acknowledgements

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