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A Design Method to Improve Temperature Uniformity on Wafer for Rapid Thermal Processing

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Received: 4 September 2018; Accepted: 21 September 2018; Published: 22 September 2018

Abstract: Single-wafer rapid thermal processing (RTP) is widely used in semiconductor manufacturing. Achieving temperature uniformity on silicon wafer is a major challenge in RTP control. In this work, a lamp configuration including five concentric lamp zones is designed to obtain uniform temperature distribution on the wafer. An optics-based model is developed to determine the optimal lamp design parameters, and a uniformity criterion is proposed to evaluate the effective irradiance distribution of the tungsten–halogen lamps on the wafer. This method can be used to determine geometric parameters of the lamp array in order to achieve uniform temperature distribution on the wafer. A realistic simulation of a cold wall RTP system with five lamp rings and a 200-mm wafer is performed. The proposed model makes way for a simple method for determining the optimal lamp design parameters in RTP systems.

Keywords: rapid thermal processing; single-wafer process; temperature uniformity; lamp configuration design

1. Introduction

The continuing downscaling of design features in ultra-large-scale integration (ULSI) is leading to manufacturing challenges in the semiconductor fabrication technology [1–4]. Hence, there is a need for better control of process parameters in order to meet the increasing demand. Thermal processes play an important role in the fabrication of semiconductor chips in the microelectronics industry. When dopant atoms are implanted into the substrate (usually by ion bombardment), the surface layers of silicon lose their crystalline structure. In order to recrystallize the surface layer and activate dopant atoms, it is necessary to anneal the wafer. Rapid thermal processing (RTP) is a technology that provides high ramp rates and short processing times for the activation of dopants with minimal redistribution combined with wafer annealing [5–8]. RTP is used for various processes during the fabrication of semiconductor devices, such as rapid thermal annealing (RTA), rapid thermal oxidation (RTO), rapid thermal chemical vapor deposition (RTCVD) and rapid thermal nitration (RTN). A typical RTP operating cycle consists of three phases: (i) a rapid heating phase to achieve a desired operating temperature, (ii) the constant-temperature processing phase, and (iii) a rapid cooling phase to cool down to ambient temperature [9]. Precise temperature control is necessary for RTP and there are several challenges that need to be addressed. Among them, maintaining uniform temperature distribution over the wafer at all times while following fast temperature trajectories is an important challenge. Numerous papers have addressed the issues related to wafer temperature control including thermal modeling, control strategy, lamp power controller, and temperature measurement [10–15]. However, most of the existing RTP systems are designed without rigorous treatment of the light flux distributions of the heating sources and their impact on wafer temperature patterns is not considered. In these approaches, the design optimization cannot be achieved until the RTP system has been constructed and tested by temperature measurements. Therefore, a predictive design method for heating sources...
(a tungsten–halogen lamp array) to achieve the temperature uniformity on wafer is desirable. In this work, the relationship between the arrangement of tungsten–halogen lamps and the uniformity of effective irradiance received by the wafer is studied, and an optimized concentric tungsten–halogen lamp array is designed. A criterion based on relative standard deviation is proposed to determine the temperature uniformity on the wafer. Simulation results show that the design yields good temperature uniformity distribution on the wafer. The proposed model makes way for a simple method for determining the optimal lamp design parameters in RTP systems.

2. Design Methodology

In this work, an axially symmetric RTP chamber is studied. A simplified schematic diagram of the RTP system is shown in Figure 1. In this system, power is supplied to several rings of tungsten–halogen lamps, and energy is transferred through a quartz window onto a thin silicon wafer via direct paths. In most RTP systems, dozens or hundreds of tungsten–halogen lamps are placed above and/or below the wafer in order to serve as the heating source. The radiation from the lamps with its central wavelength at about 900 nm heats the wafer through a selective absorption process. The temperature of wafer can be measured by thermocouples or pyrometers, and this data is used to control the output power of lamps through a feedback circuit.

![Figure 1. A simplified schematic of the rapid thermal processing (RTP) chamber. The lower frame: side-view of the RTP chamber, including a silicon wafer and a tungsten–halogen lamp array; the upper frame: bottom-view from the wafer for the configuration of the concentric tungsten–halogen lamps.](image)

For simplicity, the effect of chamber reflection and heat convection are neglected in lamp configuration design while only considering the radiative effect. The wafer is thin enough so that axial thermal gradient is neglected, and since silicon is opaque at temperature above 873 K, the silicon wafer is assumed to be a gray body at high temperatures. With these assumptions, the thermal balance equation can be expressed as,

\[ P + \varepsilon_1 \sigma T_0^4 = 2\varepsilon_2 \sigma T^4 \]  

where, the first term on the left is the effective irradiance density received by the wafer from the lamp array, the second term is the energy flow density absorbed by the wafer from the ambient (mainly including the quartz underlay), and the term on the right refers to the energy flow density.
that the silicon wafer radiates into the environment. In Equation (1), $\varepsilon_1$ and $\varepsilon_2$ are the emission coefficients of quartz and silicon respectively, $\sigma$ is the Stefan–Boltzman constant, $T_0$ and $T$ are the temperatures of quartz and wafer respectively, and the coefficient 2 indicates that the wafer has two surfaces radiating outward simultaneously. The values of these constants are listed as: $\varepsilon_1 = 0.66$, $\varepsilon_2 = 0.60$ and $\sigma = 5.672 \times 10^{-8}$ W m$^{-2}$ K$^{-4}$.

An effective lamp configuration must have the capacity to provide the required irradiative heat flux to the wafer surface for maintaining uniform temperature both during steady-state and transient heating. For this purpose, the following design principles are proposed.

(i) Concentric lamp zones. Since the wafer is circular, concentric placement of the lamps around the central axis of the wafer is an effective way to ensure temperature uniformity. A concentric circle of lamps comprises of one lamp zone, as shown in the upper frame of Figure 1. Since the lamp array is axially symmetric, only temperatures in the radial direction of the wafer are of interest by assuming axisymmetric temperature distribution on the wafer.

(ii) Linear density of lamp zone. The linear density of the $i$-th lamp zone is defined as $d_i = N_i/C_i$, where $N_i$ is the number of lamps in the zone and $C_i$ is the circumference of the zone. Here, a condition is imposed where the linear density in the outer zone is greatly or equal to the inner zone, that is $d_{i+1} \geq d_i$. This ensures that additional radiant exposure is achieved at the wafer edge to compensate for the edge heat loss.

(iii) Height of lamp array. The height of the lamp array is also an important factor affecting the temperature distribution on the wafer. In the following section, the lamp number $N$ on each zone, the radius $R$ of each zone and the height $h$ of the lamp array are three variables chosen to calculate the effective irradiance density absorbed by a point on the wafer.

(iv) Uniformity criterion. In order to determine the optimal temperature distribution on the wafer by adjusting geometric parameters ($N$, $R$ and $h$) of the lamp array, a uniformity criterion is defined for quantitative assessment. Assuming that the temperature $T$ of a point on the wafer surface depends only on the effective irradiance of all lights at that point, the uniformity criterion can be expressed by the relative standard deviation (RSD) of the effective irradiance density $P$:

$$
\delta = \sqrt{\frac{\sum_{k=1}^{n} (P_k - \bar{P})^2}{n-1}} \times 100\% 
$$

where $k$ is the index of a point on a given radius of the wafer surface (a total of $n$ points is evenly distributed on this radius), $P_k$ is the effective irradiance density absorbed by the $k$-th point, and $\bar{P}$ is the average value of the effective irradiance densities at all points on this radius. According to this criterion, the temperature distribution on the wafer can be considered to be uniformity when the RSD reaches a minimum, $\delta_{\text{min}}$. The corresponding geometric parameters for the optimal design can then be obtained.

3. Problem Formulation

In this section, an optics-based approach is formulated in order to solve the temperature uniformity problem. A cylindrical coordinate system is used in which the origin (point $O$) is at the center of the wafer upper surface, the $OZ$-axis coincides with the central axis of the wafer, and $Op$ is the pole axis, as shown in Figure 2. A ray from a point light source $S$ (i.e. one point on a lamp zone) hits a point $x$ on a given radius of the wafer upper surface, and then it is reflected and refracted at the point $x$, as shown in the inset of Figure 2. The point $P$ is the projection of the source $S$ on the wafer, $\theta$ is the angle between the lines $Ox$ and $OP$, and $a$ and $\beta$ are the incidence and reflection angles.
respectively. Assume that \( h = \mathbf{SP}, R = \mathbf{OP}, r = \mathbf{Ox} \). According to the optics theory [16], the irradiance density received by a point \( x \) from a point light source \( S_{ij} \) is expressed by:

\[
P_{ij} = \frac{W_{ij}}{4\pi} \frac{h}{(r^2 + R_i^2 + h^2 - 2rR_i \cos \theta_{ij})^{\frac{3}{2}}}
\]

where \( W_{ij} \) is the power of the \( j \)-th lamp on the \( i \)-th lamp zone. The total irradiance density received by the point \( x \) (the \( k \)-th point on the given radius) is:

\[
P_k = \sum_{i} \sum_{j} (\eta_{ij} \cdot P_{ij})
\]

where \( \eta_{ij} \) is the absorption coefficient. The absorption coefficient accounts for the fact that not all the irradiance that reaches the point can be absorbed. Since the wafer is assumed to be a grey body hereinabove, it is considered that all the light that is refracted into the wafer can be absorbed. Thus, based on the Fresnel formulae, the absorption coefficient is given by:

\[
\eta_{ij} = \frac{1}{2} \cdot \left( \frac{1}{n_{Si}} |(t_1)_{ij}|^2 + n_{Si} |(t_2)_{ij}|^2 \right)
\]

where \( t_1 \) and \( t_2 \) are the parallel and vertical components of the amplitude transmissivity of the refracted light respectively, \( n_{Si} \) is the refractive index of silicon. The coefficient 1/2 is introduced because the incidence rates in both parallel and vertical directions to the wafer surface are normalized to 1. The parameters \( t_1 \) and \( t_2 \) are expressed by:

\[
t_1 = \frac{2 \cos \alpha}{n_{Si} \cos \alpha + \cos \beta} \quad t_2 = \frac{2 \cos \alpha}{\cos \alpha + n_{Si} \cos \beta}
\]

Figure 2. A sketch of the geometrical relationship for the wafer irradiated by a tungsten–halogen lamp. The inset shows the reflection and refraction of a ray incident on the silicon wafer.

For convenience, we assume that all the lamps have the same power, \( W \). The reduced effective irradiance density, \( L_k \), is introduced as:

\[
L_k = \frac{4\pi}{W} P_k
\]

Equation (2) can then be rewritten as:

\[
\delta = \sqrt{\frac{\sum_{j=1}^{n} (t_{ij} - \tau)^2}{n - 1}} \times 100\%
\]
where $\bar{L}$ is the average reduced effective irradiance density.

4. Design Procedure and Example

In the design of a RTP system, the effective illumination uniformity from a lamp array is a prerequisite in order to achieve temperature uniformity. Poor placement of lamp array can result in an increase in temperature difference, and the temperature uniformity cannot be improved regardless of how the RTP system is controlled. In this section, based on the proposed optimization methodology, a cold wall RTP system with five lamp rings and a 200 mm wafer is considered as an example to design an optimal tungsten–halogen lamp array. For simplicity, unless further specified, units of all the geometric parameters are mm in this section. The radii of the 1st, 2nd, 3rd, 4th and 5th rings of the lamp array are marked as $R_1, R_2, R_3, R_4$ and $R_5$, respectively, and they are grouped into a matrix $R = (R_1, R_2, R_3, R_4, R_5)$. Similarly, the lamp number of the 1st, 2nd, 3rd, 4th and 5th rings of the lamp array are marked as $N_1, N_2, N_3, N_4$ and $N_5$, respectively, and they are grouped into a matrix $N = (N_1, N_2, N_3, N_4, N_5)$.

The design procedure is summarized in the following steps.

Step 1: Initialization. Select a set of data in Ref. [17] as the initialization condition with $R = (0, 32, 64, 96, 128)$, $N = (1, 6, 12, 19, 26)$, as listed in Table 1.

| Step | $R$ | $N$ | $h$ | $\delta_{\text{min}}$ |
|------|-----|-----|-----|------------------|
| 1    | (0 32 64 96 128) | (1 6 12 19 26) | 34 | 4.07% |
| 2    | (0 32 64 96 128) | (1 6 14 24 40) | 58 | 0.727% |
| 3    | (0 32 64 96 128) | (1 6 12 23 45) | 66 | 0.473% |
| 4    | (0 32 63 96 128) | (1 6 12 23 45) | 64 | 0.396% |

Step 2: Optimizing $N$ & $h$. Keep $R$ constant, change $N_3, N_4,$ and $N_5$ as a function of $h$ sequentially, and determine RSD to seek its minimum value.

Step 3: Refining $N$. Repeat Step 2 and continue to refine the values of $N$ and $h$.

Step 4: Optimizing $R$ & $h$. Keep $N$ constant, change $R_2, R_3, R_4,$ and $R_5$ as a function of $h$ sequentially, and determine RSD to seek its minimum value.

Step 5: Analyzing the results. Analyze the results obtained in the above steps, and provide the optimal design parameters of the tungsten–halogen lamp array.

Table 1 summarizes the results obtained in Step 1, 2, 3, and 4. In the initialization condition, the RSD of the effective irradiance density on the wafer decreases rapidly and then increases gradually as the height of the lamp array is increased, as shown in the upper frame of Figure 3.

For the first step, with the initialization values, a minimum of RSD is obtained as $\delta_{\text{min}} = 4.07\%$ at $h = 34$ mm. From this result, it can be inferred that achieving a uniform temperature distribution on the wafer could be challenging due to the larger RSD value.

In Step 2, $R$ is kept constant and $N_2$ vs. $h$ is carried out to find $\delta_{\text{min}}$. A $\delta_{\text{min}} = 3.33\%$ is obtained when $h = 32$, $R = (0, 32, 64, 96, 128)$ and $N = (1, 6, 14, 19, 26)$. Further, changing $N_3$ vs. $h$ yields a $\delta_{\text{min}} = 1.11\%$ when $h = 40$, $R = (0, 32, 64, 96, 128)$ and $N = (1, 6, 14, 24, 26)$. Finally, changing $N_4$ vs. $h$ gives a $\delta_{\text{min}} = 0.727\%$ when $h = 58$, $R = (0, 32, 64, 96, 128)$ and $N = (1, 6, 14, 24, 40)$, as listed in Table 1 and shown in the lower frame of Figure 3.

The third step and the fourth step are fine tuning processes, with only minor changes in the geometric parameters and the minimum values of RSD, as shown in the Table 1 and Figure 3. The final results are obtained with $h = 64$, $R = (0, 32, 63, 96, 128)$, $N = (1, 6, 12, 23, 45)$, and $\delta_{\text{min}} = 0.396\%$. The linear densities of lamps on these lamp rings is also calculated, and the results are $d = (N/A 0.030 0.030 0.038 0.056)$, which is in accordance with the second rule in Section 2. The linear density of the fifth lamp ring is the
largest, which is beneficial to compensate for the heat loss near the edge of the wafer and to achieve better uniformity of the temperature distribution on the wafer.

![Figure 3](image_url)

**Figure 3.** The relative standard deviation vs. the height of lamp array. The upper frame: RSD vs. the height of lamp array at the initialization condition; the lower frame: RSD vs. the height of lamp array after Step 2, 3 and 4, respectively.

The minimum of RSD is a sufficient condition in determining the uniform distribution of the effective irradiance received by the wafer. Figure 4 shows the minimum values of RSD determined from each sub-step of the lamp array design. It can be seen from Figure 4 that $\delta_{\text{min}} = 4.07\%$ initially, and then decreases rapidly during the Step 2. During Step 3 and 4, the $\delta_{\text{min}}$ changes gradually, especially in the last three sub-steps, it stabilizes to 0.396%. This indicates that a certain degree of uniform effective irradiance distribution on the wafer has been attained and the optimized geometric parameters of lamp array can be extracted.

![Figure 4](image_url)

**Figure 4.** The minimum, $\delta_{\text{min}}$, of RSD of effective irradiance density during each sub-step of optimal design.

Next, the power of tungsten–halogen lamps required at a given annealing temperature is estimated based on the geometrical parameters of the lamp array obtained from the optimization procedure. First, the relative irradiance density is calculated by substituting the geometric parameters, $h = 64$, $R = (0,32,63,96,128)$, and $N = (1,6,12,23,45)$, into Equations (3) and (4). Then, under the ambient temperature setting, $T_0$, the power of tungsten–halogen lamp can be obtained according to Equation (1). Here, the term $2\varepsilon_1 a T_0^4$ in Equation (1) originates from the thermal energy of the quartz underlay and
the heat of the gas inside the chamber, which can be determined by measurement. Figure 5 shows the relationship between the power of tungsten–halogen lamp and the annealing temperature of silicon wafer at $T_0 = 300, 400, 500, 600, 700,$ and $800$ K. The influence of ambient temperature on the power of tungsten–halogen lamp is relatively small, as evident from Figure 5. In order to better observe the trends, a partially enlarged section near $1000^\circ$C is shown in the lower-right inset of Figure 5. The top-left inset of Figure 5 shows the lamp power vs. the ambient temperature for the annealing temperature $850^\circ$C and $1000^\circ$C, respectively. This data will help to compile the program stored in E$^2$PROM of RTP system to control the temperature of wafer. For instance, on the condition of $T_0 = 300$ K, when the annealing temperature is set to be $850^\circ$C, the required power of each lamp will need to be $1.43$ kW; or when the annealing temperature is set to $1000^\circ$C, the required power of each lamp needs to be $2.36$ kW.

![Figure 5](image_url)

**Figure 5.** The lamp power vs. the wafer temperature at different ambient temperature. The top-left inset: the lamp power vs. the ambient temperature for the annealing temperature $1123$ K ($850^\circ$C) and $1273$ K ($1000^\circ$C); the lower-right inset: enlarged view near the wafer temperature of $1000^\circ$C.

5. Conclusions

A lamp configuration design method is proposed for achieving temperature uniformity of a RTP system. The central idea here is to optimize the geometrical parameters, including the radius of each lamp ring, the lamp number on each lamp ring and the height of lamp array, so as to minimize the variation of the effective irradiance received by the silicon wafer. An optics-based model is developed to determine the optimal lamp design parameters, and a uniformity criterion is introduced to evaluate the effective irradiance distribution of the tungsten–halogen lamps on the wafer. The efficacy of the design method is demonstrated through a design example in which the optimal geometrical parameters, $h = 64$, $R = (0,32,63,96,128)$, and $N = (1,6,12,23,45)$, are obtained for a cold wall RTP system with five lamp rings and a $200$ mm wafer. The linear density of the outmost lamp ring needs to be the largest, which is beneficial to compensate for the heat loss near the edge of the wafer. Additionally, this method can also be used in the design of a RTP system with a $300$ mm wafer. Based on the thermal balance equation presented in this work, the power of tungsten–halogen lamps required at a given annealing temperature can be determined, and this data can be integrated within the E$^2$PROM of RTP system to control the temperature of wafer. In a practical setting, it may be necessary to explore both the open-loop and feedback control to evaluate the merit of the lamp design.

**Author Contributions:** H.-G.Y. developed the concept; P. H. designed and simulated the system; H.-G.Y. analyzed the data and wrote the paper.

**Funding:** This research was funded by the National Natural Science Foundation of China (Grant No. 61474041) and the Technology Program of Changsha (No. KQ1703001).
Acknowledgments: We gratefully acknowledge financial support from the National Natural Science Foundation of China (Grant No. 61474041) and the Technology Program of Changsha (No. KQ1703001). The authors would like to thank Cheng Xu of Shenzhen SI Semiconductors Co. LTD for his helpful discussions.

Conflicts of Interest: The authors declare no conflict of interest.

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