AGE AND DISTANCE FOR THE OLD OPEN CLUSTER NGC 188 FROM THE ECLIPSING BINARY MEMBER V 12

Søren Meibom1,6, Frank Grundahl2, Jens Vigo Clausen3, Robert D. Mathieu3, Søren Frandsen2, Andrzej Pigulski4, Artur Narwid4, Marek Steslicki4, and Karolien Lefever5

1 University of Wisconsin–Madison, WI, USA; smeibom@cfa.harvard.edu
2 Department of Physics and Astronomy, Aarhus University, Denmark
3 Niels Bohr Institute, Copenhagen University, Denmark
4 Instytut Astronomiczny Uniwersytetu Wrocławskiego, Kopernika 11, 51-622 Wrocław, Poland
5 Instituut voor Sterrenkunde, Katholieke Universiteit Leuven, 3001 Heverlee, Belgium

Received 2008 December 9; accepted 2009 March 26; published 2009 May 12

ABSTRACT

We present time series radial velocity, and photometric observations of a solar-type double-lined eclipsing binary star (V 12) in the old open cluster NGC 188. We use these data to determine the spectroscopic orbit and the photometric elements for V 12. From our analysis, we determine accurate masses ($M_p$, $M_s$), $M_r$, and radii ($R_p$, $R_s$, $R_r$) for the primary and secondary binary components. We adopt a reddening of $E_{B-V} = 0.087$ for NGC 188, and derive component effective temperatures of $5900 \pm 100$ K and $5875 \pm 100$ K, respectively, for the primary and secondary stars. From their absolute dimensions, the two components of V 12 yield identical distance moduli of $V_0 - M_V = 11^{m}024 \pm 0^{m}09$, corresponding to $1770 \pm 75$ pc. Both stars are near the end of their main-sequence evolutionary phase, and are located at the cluster turnoff in the color–magnitude diagram. We determine an age of $6.2 \pm 0.2$ Gyr for V 12 and NGC 188, from a comparison with theoretical isochrones in the mass–radius diagram. This age is independent of distance, reddening, and color–temperature transformations. We use isochrones from Victoria–Regina (VRSS) and Yonsei–Yale (Y2) with [Fe/H] = −0.1 and [Fe/H] = 0.0. From the solar metallicity isochrones, an age of 6.4 Gyr provides the best fit to the binary components for both sets of models. For the isochrones with [Fe/H] = −0.1, ages of 6.0 Gyr and 5.9 Gyr provide the best fits for the (VRSS) and (Y2) models, respectively. We use the distance and age estimates for V 12, together with best estimates for the metallicity and reddening of NGC 188, to investigate the locations of the corresponding VRSS and Y2 isochrones relative to cluster members in the color–magnitude diagram. Plausible changes in the model metallicity and distance to better match the isochrones to the cluster sequences, result in a range of ages for NGC 188 that is more than 3 times that resulting from our analysis of V 12.

Key words: binaries: eclipsing – binaries: spectroscopic – open clusters and associations: general – open clusters and associations: individual (NGC 188) – stars: evolution – techniques: photometric – techniques: spectroscopic

Online-only material: machine-readable and VO tables

1 INTRODUCTION

NGC 188, once thought to be the oldest open cluster in our Galaxy (e.g., Sandage 1962), represents the old stellar population of the Galactic disk. Due to its richness, location in the Galaxy (α2000 = 0°47′, δ2000 = +85°15′; l = 122°8, b = 22°4), large population of single and binary members (Platais et al. 2003; Geller et al. 2008), and its age, NGC 188 is a benchmark cluster for studies of stellar evolution and cluster dynamics, and for the formation and chemical and dynamical evolution of the Galactic disk. Determining an accurate and precise age for NGC 188 is of general importance.

The age determined for NGC 188 has changed dramatically since the early determination by Sandage (1962) of 14–16 Gyr. Later studies derived 9–12 Gyr (Demarque & Larson 1964; Iben 1967), and more recent values range from ~6 Gyr (Twarog &Anthony-Twarog 1989; Caputo et al. 1990; Demarque et al. 1992; Meynet et al. 1993; Dinescu et al. 1995) to ~7–8 Gyr (Hobbs et al. 1990; Sarajedini et al. 1999; VandenBerg & Stetson 2004). Past age estimates were based on fitting model isochrones to the cluster’s main-sequence, turnoff, and giant branch in the color–magnitude diagram (CMD). Ages derived using this “isochrone method” are sensitive to uncertainties in cluster extinction and reddening, as well as in the conversions between model (bolometric luminosity, temperature) and observed (apparent luminosity, color) quantities.

For NGC 188, the values for reddening and metallicity are well constrained. A reddening of $E(B-V) = 0^{m}087$ derived from the Schlegel et al. (1998) dust maps agrees with the estimates of Sarajedini et al. (1999) of $0^{m}09 \pm 0^{m}02$ from their two-color diagram. We use $E(B-V) = 0^{m}087$ throughout this paper. The metallicity of NGC 188 has been studied during the last two decades (e.g., Hobbs et al. 1990; Friel & Janes 1993; Friel et al. 2002; Randich et al. 2003; Worthey & Jowett 2003). Results from photometric studies agree with results from medium- to high-resolution spectroscopy, both of which find the cluster’s metallicity to be in the range from [Fe/H] = −0.12 to solar. Estimates of the cluster distance from isochrone fitting to the CMD have over the past decade agreed to within a few percent, ranging from 1660 pc to 1710 pc (Sarajedini et al. 1999; VandenBerg & Stetson 2004; Bonatto et al. 2005; Fornal et al. 2007) with individual uncertainties of the order of 5%.
NGC 188 is a key cluster of the WIYN\(^7\) Open Cluster Study (WOCS; Mathieu 2000). As part of WOCS, Geller et al. (2008) present a time-series radial-velocity survey of more than 1046 stars in the field of NGC 188 over a time baseline of eleven years. In combination with a deep proper-motion study of the cluster (Platais et al. 2003), the WOCS spectroscopic data have securely identified large populations of single and binary cluster members. V12 was established as a double-lined spectroscopic binary and confirmed as a cluster member early in the WOCS survey. The eclipsing nature of the system was discovered by Zhang et al. (2002) in a time-series photometric survey for variable stars. Zhang et al. (2002) recorded only one complete eclipse and classified V12 as an Algol-type eclipsing binary. The photometry used by Zhang et al. (2002) located V12 at the foot of the giant branch in the NGC 188 CMD. A later photometric survey by Zhang et al. (2004) placed V12 above the cluster turnoff in the CMD, and estimated the period of V12 to be 2.8 days. Just recently, V12 was identified as a detached eclipsing binary in NGC 188 by Mochejska et al. (2008). They determine a period of 2.9 days.

As a spectroscopic double-lined and eclipsing binary, precise masses and radii can be determined for the primary and secondary components of V12. Because both components are near the turnoff mass for NGC 188, a comparison of their masses and radii to theoretical isochrones can put tight constraints on the age of the binary, and thus its parent cluster. Importantly, the determinations of the masses and radii are independent of the reddening, distance, and metallicity of the system. In addition, double-lined eclipsing binaries are excellent primary distance indicators (e.g., Guinan et al. 1998; Clausen 2004). Therefore, the analysis of eclipsing binary stars, in particular when coupled with reliable information about the stellar chemical composition, is important to improving our understanding of the physical properties and evolution of stars. However, stellar evolution models have progressed to a level where stellar parameters must be observed with a precision of \(\lesssim 1\%\) or better to provide useful constraints (e.g., Andersen 1991). For examples of detailed analysis of field binaries and the comparisons with stellar evolution models see, e.g., Torres et al. (2006), López-Morales & Shaw (2007), and Clausen et al. (2008). While bright eclipsing binaries in relatively nearby clusters have been observed for decades (Kraft & Landolt 1959; Semenik 1962; Sahade & Davila 1963; Popova & Kraicheva 1984; Clausen & Giménez 1987; Giménez & Clausen 1996), and several studies have been published recently (see, e.g., Southworth et al. 2005 and Southworth & Clausen 2006 and references therein), it is only recently that fainter systems in more distant clusters have been discovered and published (e.g., Kaluzny et al. 2006; Grundahl et al. 2008).

In Section 2, we begin the analysis of the spectroscopic data on V12. We determine the orbital elements of V12 and give the probabilities for it being a kinematic member of NGC 188. Section 3 describes the photometric data, the light curves, and the photometric elements of the V12 components. That leads to our determination of the physical parameters for V12, including effective temperature, distance, and age, in Section 4. In Section 5, we examine how well the isochrones that best fit the V12 components represent the rest of the cluster members in the NGC 188 CMD, and we compare the cluster age determined via V12 to those determined by the isochrone method. In Section 6, we summarize our results and give our conclusions.

2. RADIAL VELOCITIES AND SPECTROSCOPIC ELEMENTS OF V12

2.1. Spectroscopic Observations and Data Reduction

A detailed description of the spectroscopic observations and radial velocity measurements of stars in NGC 188 can be found in Geller et al. (2008). The spectroscopic observations of V12 were acquired from 1996 September to 2001 July with the WIYN telescope and the Hydra multiobject spectrograph in a single 250-Å wide echelle order centered on 5130 Å and with a resolution of \(\sim 20,000\). For each observation, three 40 minute exposures were combined to increase the signal-to-noise ratio of the spectrum and to filter out cosmic-ray events. The CCD bias level was determined using the overscan section of the chip and subtracted. A single domeflat exposure, adjacent in time to the science exposures, was used for the purposes of tracing and extracting the stellar spectrum, flat-field correction, and fiber throughput correction. The three consecutive science exposures were bracketed by thorium–argon (ThAr) comparison lamp exposures used to define the pixel-to-wavelength mapping (dispersion solution). The DOHYDRA\(^8\) IRAF task was used for the reduction of the WIYN/Hydra multispectra data. The signal-to-noise ratio (S/N) for the 16 spectra used for the orbital solution of V12 ranges from \(\sim 15–25\) per resolution element (2 pixels) of \(\sim 14\) km s\(^{-1}\). For single-lined stars with slow to moderate rotation velocities, radial velocities with a precision of \(\lesssim 0.4\) km s\(^{-1}\) (Geller et al. 2008) were derived from the spectra via cross correlation with a high S/N sky (solar) spectrum obtained at evening twilight.

2.2. Component Radial Velocities and Orbital Elements

Because we seek maximum precision and accuracy for the V12 velocities, we have used two methods to independently re-reduce the spectra and derive velocities for both components. First, we have determined radial velocities using the two-dimensional cross-correlation algorithm TODECOR (Zucker & Mazeh 1994). For the TODECOR analysis, we have used identical synthetic templates for the two binary components, since they are nearly identical; see Section 4. The templates were calculated from the Synplot/Synspec\(^9\) tool by Hubeny & Lanz for \(T_{\text{eff}} = 6000\) K, \(\log(g) = 4.0\), [Fe/H] = 0.0, \(v\sin i = 20.0\) km s\(^{-1}\), and a resolution of \(R = 20,000\), adopting an ATLAS9 model atmosphere (Kurucz 1993). Preliminary spectroscopic elements were calculated from the measured radial velocities using the method of Lehman–Filhés implemented in the SBOP program (Ettel 2004). The orbital period was adopted from Equation (2) (Section 3.3). The orbit was assumed to be circular based on an initial eccentricity of 0.005 ± 0.003. Because spectral lines of the stars move in and out of the observed spectral range with orbital phase, it is necessary to apply corrections to the radial velocities derived from the TODECOR algorithm (e.g., Torres et al. 1997 and Torres & Ribas 2002). To determine such corrections, we have constructed synthetic binary spectra from the template, adopting for each orbital phase the radial velocity shifts defined by the preliminary elements. These synthetic spectra were

\(^{7}\) The WIYN Observatory is a joint facility of the University of Wisconsin–Madison, Indiana University, Yale University, and the National Optical Astronomy Observatories located at Kitt Peak National Observatory, AZ, USA.

\(^{8}\) http://iraf.noao.edu/tutorials/dohydra/dohydra.html

\(^{9}\) http://nova.astro.umd.edu/Synspec43/synspec.html
then analyzed by TODCOR in the same manner as the observed V 12 spectra. The corrections (i.e., measured–calculated velocities for the synthetic binary spectra), which are shown in Figure 1, are then added to the measured V 12 velocities and revised spectroscopic elements are determined from SBOP. In the case of V 12, we find that the radial velocity corrections are quite significant, up to 3 km s$^{-1}$ for both components. Including the corrections improves the fit of the theoretical orbit to the radial velocities significantly, and the effect on the absolute masses is not negligible (≈2% for both components). The final velocities including corrections are listed in Table 1, and the corresponding spectroscopic elements are given in Table 2.

The final spectroscopic orbital solution for V 12 is shown in Figure 2. Within the errors, separate analysis of the radial velocities for the primary and secondary components, respectively, yields identical elements. Also, analysis performed with several other templates ($v \sin i = 10.0$ km s$^{-1}$, corresponding to synchronous rotation—see Section 4.2—200 K lower temperatures; different spectrum code, Valenti & Piskunov 1996, and line list, Kupka et al. 1999) produces indistinguishable results.

Second, we have applied spectral disentangling. This technique solves simultaneously for the contributions of the components to the observed composite spectra, and for the Doppler shifts in the component spectra. We have applied the method introduced by Simon & Sturm (1994) using a version of the original code revised for the Linux operating system. It assumes a constant light level outside eclipses, which is fulfilled for V 12. Dedicated IDL$^{10}$ programs were applied to remove cosmics ray events and other defects, and for normalization of the spectra before these analysis. Spectral disentangling is applicable because sufficient (16) WIYN spectra ($S/N \approx 15–25$) are available giving good phase/velocity coverage outside eclipses. We have assumed the ephemeris given in Equation (2) (Section 3.3) and fitted for the velocity semi-amplitudes of the spectroscopic orbit for each component. We obtain $K_p = 73.0$ km s$^{-1}$ and $K_s = 74.7$ km s$^{-1}$, i.e., excellent agreement with the results given in Table 2. We have not quoted uncertainties for the semi-amplitudes, since it is not clear how to calculate robust values in the disentangling analysis (Hynes & Maxted 1998). The disentangled spectra have $S/N$ ratios of $\approx 60$ and cover 200 Å.

2.3. Cluster Membership Probabilities for V 12

The center of mass radial velocity of V 12 is $-40.0 \pm 0.1$ km s$^{-1}$ (Table 2). From the WOCS radial velocity survey of NGC 188 Geller et al. (2008) report an average cluster velocity of $-42.36 \pm 0.04$ km s$^{-1}$. The center of mass velocity of V 12 is $2.5\sigma$ from the fitted cluster mean, corresponding to a radial velocity membership probability of 50%. A 97%

---

$^{10}$ http://www.itvis.com/ProductServices/IDL.aspx
astrometric membership probability was determined for V12 from the proper motion study of Platais et al. (2003).

3. PHOTOMETRY OF V12

The photometric data for V12 consist of $V$ and $I_C$ CCD observations obtained at the 2.56 m Nordic Optical Telescope (NOT) 2004 July–2005 April, at the 1.2 m Flemish Mercator Telescope 2005 April, and at the 0.6 m telescope at Bialkow observatory in Poland 2005 February–2005 April. At the NOT, either StanCam or ALFOSC was used; we refer the reader to the telescope homepages for further information. Table 3 gives a summary of the data obtained.

At each telescope, the flat fields used in the data reduction were obtained during evening twilight. All photometry was carried out with DAOPHOT/ALLSTAR (Stetson 1987) and DAOphot (Stetson 1990) and transformed to a common coordinate system using MATCH and MASTER (P. Stetson 2006, private communication). For each frame, we produced a point-spread function (PSF) using the brightest stars in the field and subsequently carried out aperture photometry in large apertures (neighbor stars subtracted), using the NEDA routine provided with DAOPHOT. Subsequently, the aperture photometry was fed into DAOphot to obtain the final large-aperture magnitudes. We found that this procedure gave slightly better photometric precision than using profile-fitting photometry.

3.1. Transformation to $V$ and $I_C$

For the analysis of the light curve, it is important that all data in a given band are on the same photometric system. For this purpose, we used the photometry provided by Stetson et al. (2004) which gives calibrated $UBVR$ photometry for a large fraction of the stars in NGC 188. We note that $R$ and $I$ are on the Cousins system. The stars in common with Stetson et al. (2004) were then used as local standards and the following transformation equations was adopted (for both $V$ and $I$):

$$m_{\text{obs}} = M_{\text{std}} + \alpha \times (B-I)_{\text{std}} + \beta.$$ (1)

Capital letters denote the calibrated magnitudes and lower case refers to the instrumental magnitudes. For each combination of telescope, instrument, and filter, the values of $\alpha$ and $\beta$ were found by the following procedure: (1) we fitted Equation (1) to the data from each frame (excluding V12 which is variable); (2) we calculated the average value of $\alpha$, as it is expected to be constant in time; (3) using the average value for $\alpha$, the values of $\beta$ were re-determined as the final frame zero point ($\beta$).

Using these values, we calculated $V$ and $I_C$ magnitudes for V12. In the calculation of the zero points, stars with $(B-I)$ in the interval between 1.2 and 2.6 were used. Most of the stars had a color within $\pm 0.3$ mag of V12. Thus, the zero points are essentially based on stars of very similar color to $V_{12}$, i.e., stars similar to the turnoff color of NGC 188.

Before combining the photometry and adjusting zero points (see Section 3.2), we formed mean values of the out-of-eclipse observations of V12 from ALFOSC and StanCam in order to obtain a higher precision than obtained by Stetson et al. (2004). This is important for the determination of effective temperatures and distances. Rms errors of about 0.005 magnitudes were obtained, compared to 0.013 ($V$) and 0.018 ($I$) for Stetson et al. (2004). The mean $V$ magnitudes from the two instruments agreed, whereas a difference of about 0.02 magnitudes was seen in $I$. We adopt the following out-of-eclipse results for V12: $V = 14.745 \pm 0.005$, $I = 13.951 \pm 0.010$, $V - I = 0.794 \pm 0.011$.

3.2. V12 Light Curves

When combining calibrated photometry from several detector/filter combinations the photometric scale and zero points are always a concern. We therefore compared the phased light curves to check their quality. We therefore calculated the phased light curve to check its quality. We therefore calculated the phased light curve to check its quality. We therefore calculated the phased light curve to check its quality.

Figure 2. Spectroscopic orbital solution for V12 and radial velocities listed in Table 1 (filled circle: primary; open circle: secondary). The horizontal dotted line (upper panel) represents the center-of-mass velocity of the system. Phase 0.0 corresponds to central primary eclipse.

Table 3 (filled circle: primary; open circle: secondary). The horizontal dotted line (upper panel) represents the center-of-mass velocity of the system. Phase 0.0 corresponds to central primary eclipse.

| Telescope      | $N_V$ | $N_I$ | $t_{\exp}(V)$ | $t_{\exp}(I)$ |
|----------------|-------|-------|----------------|----------------|
| NOT/StanCam    | 131   | 118   | 120            | 90             |
| NOT/ALFOSC     | 197   | 189   | 60             | 45             |
| Mercator       | 0     | 40    | ...            | 180            |
| Bialkow        | 51    | 36    | 300            | 200            |

For the analysis of a large data set for the old open cluster NGC 6791 but note that Stetson et al. (2003) carried out an extensive analysis of a large data set for the old open cluster NGC 6791 and found that combining calibrated photometry from different telescope/filter/CCD combinations and different nights can exhibit scatter of the order of $0.002$. We note that the $I$ flat field of ALFOSC contains relatively large gradients near the center of the field where V12 is located in our images. This instrument is a combined focal reducer and the spectograph, and the gradient seen is probably due to sky concentration. We speculate that this is related to the offsets between the ALFOSC and StanCam
Figure 3. Observed $V$ light curve of V12 (upper panel, crosses) and the theoretical EBOP light curve (line) corresponding to the photometric solution presented in Table 5 assuming linear limb darkening coefficients by Van Hamme (1993). ($O-C$) residuals of the observations from the theoretical light curve are shown in the two lower panels.

Figure 4. Observed $I$ light curve of V12 (upper panel, crosses) and the theoretical EBOP light curve (line) corresponding to the photometric solution presented in Table 5 assuming linear limb darkening coefficients by Van Hamme (1993). ($O-C$) residuals of the observations from the theoretical light curve are shown in the two lower panels.

### Table 4

| HJD−2,400,000 | rms    | Type | $O-C$/Phase | Band   |
|---------------|--------|------|-------------|--------|
| 50906.03886   | 0.00276| ⋯    | 0.00003     | Spectroscopic orbit |
| 53221.56770   | 0.00052| P    | −0.00083    | $I$    |
| 53221.56854   | 0.00053| P    | 0.00001     | $V$    |
| 53229.61958   | 0.00022| P    | −0.00051    | $I$    |
| 53229.62044   | 0.00011| P    | 0.00035     | $V$    |
| 53312.62875   | 0.00019| P    | 0.00007     | $I$    |
| 53312.62954   | 0.00015| P    | 0.00086     | $V$    |
| 51605.25      | 0.01   | S    | 0.49989     | Zhang et al. (2001) |
| 53452.47085   | 0.00028| S    | 0.49997     | $I$    |
| 53452.47109   | 0.00010| S    | 0.50000     | $V$    |
| 53465.48005   | 0.00047| S    | 0.50006     | $I$    |
| 53465.48001   | 0.00060| S    | 0.50005     | $V$    |

**Note.** $O-C$ values for primary (P) and phases for secondary (S) minima are calculated for the ephemeris given in Equation (2).

Data. Offsets of similar size were found for the Mercator and Bialkow data in I.

Since the internal precision of our data is significantly better than 0.01, we decided to adjust the zero points on a nightly basis for both the $V$ and $I$ data in order to produce a phased light curve with the smallest amount of scatter. To do this, we first decided to adopt the values of $V$ and $I$ from Stetson et al. (2004) so as to set magnitudes for V12, since this is well calibrated and multi-epoch photometry (at random phases for V12). For each night with photometric data out (or partly out) of eclipse, we adjusted the zero point to the values of Stetson et al. (2004). Using the phased data, small offsets were then applied to the remaining light curve segments.

It is important to emphasize that the depths of the eclipses of the final light curves are the same as observed with the different instruments. The data from Bialkow, NOT/StanCam, and NOT/ALFOSC cover parts of the eclipse which include the central eclipse and out-of-eclipse data, and the observed eclipse depths in these agree from 0.01 to 0.02. We also note that for the analysis of the light curve the absolute level of the out-of-eclipse part does not have any influence. This only enters into the determination of the absolute magnitude of the stars (or equivalently the cluster distance modulus). The out-of-eclipse data from NOT show a scatter around a constant level of 3.4 mmag for both the $V$ and $I$ filter.

The light curves are shown in Figures 3 and 4. A total of 379 and 383 measurements were obtained in $V$ and $I$, respectively. Both eclipses have been covered on several nights, and there are enough data points outside eclipses to define the maximum light level because V12 is so well detached that essentially no out-of-eclipse variations are present. The eclipses are narrow and of almost identical depths (about 0.6 mag in V). They are of the same duration, and secondary eclipse occurs at phase 0.5, consistent with a circular orbit.

As a final note, we point out that the V12 field is uncrowded and the stars are bright. This means that it should be a fairly easy task to obtain even better data than presented here. To avoid the transformation difficulties encountered here, this should be done using a single telescope/detector/filter combination for each band.

### 3.3. Times of Minimum and Ephemeris

From the $V$ and $I$ light-curve observations, 6 times of primary minimum and 4 times of secondary minimum have been derived. They are given in Table 4 together with the time of primary
minimum obtained from the spectroscopic orbit (see Section 2) and the approximate time of secondary minimum by Zhang et al. (2004). When possible, the method of Kwee & van Woerden (1956) was applied, otherwise a second-order polynomial was fitted to the observations.

An unweighted linear least-squares fit to the times of primary minimum yields the following ephemeris:

\[
\text{Min I} = \text{HJD 2453299.62009} + 6.5042969 \times E
\]

\[\pm 25 \pm 18, \] (2)

which we adopt for the light curve and radial velocity analysis. Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis. Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis. Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis.

Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis. Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis. Within errors, the times of secondary minimum give the same which we adopt for the light curve and radial velocity analysis.

3.4. Photometric Elements

The choice of the binary model for light-curve analysis depends strongly on the relative radii of the components and the irradiation between them. In our case, the system is well detached with relative radii below 0.1, the components are little deformed (oblateness of 0.0006) and reflection effects are small. Therefore, the simple Nelson-Davis-Etzel model (Nelson & Davis 1972; Etzel 1981; Martynov 1973), which represents the deformed stars as biaxial ellipsoids and applies a simple bolometric reflection model, is expected to be adequate.

We have adopted the corresponding EBOP code (Popper & Etzel 1981), supplemented by an extended version JKTEBOP including Monte Carlo simulations for the analysis and the assignment of realistic errors for the photometric elements; see, e.g., Southworth et al. (2004a, 2004b).

We have analyzed the V and I light curves independently, and for each band identical weights have been assigned to all observations. A photometric scale factor (the magnitude at quadrature) was always included as an adjustable parameter, and the phase of primary eclipse was allowed to shift from 0.0. The mass ratio between the components was kept at the spectroscopic value. Gravity darkening coefficients corresponding to convective atmospheres were applied in accordance with the effective temperatures derived below, and the simple bolometric reflection model built into EBOP was used. Linear limb darkening coefficients were either assigned from theoretical calculations (Van Hamme 1993; Claret 2000) according to the effective temperatures, surface gravities, and abundances, or included as adjustable parameters.

In tables and text on photometric solutions we use the following symbols: \(i\) orbital inclination; \(r\) relative radius; \(k = r_s/r_p\); \(r\) linear limb darkening coefficient; \(\gamma\) gravity darkening coefficient; \(J\) central surface brightness; \(L\) luminosity.

EBOP solutions for V 12 are shown in Table 5. The following parameters were adjusted: \(i, r_p, k, J, J_p\), and as seen their formal errors are quite small. For each band, the solutions for the different assumptions on limb darkening agree well, and also differences between the V and I solutions are small. The adjusted linear limb darkening coefficients are close to those by Van Hamme (1993), whereas those by Claret (2000) are about 0.1 higher in both bands.

In order to assign realistic errors to the photometric elements, we have supplemented the analysis with EBOP solutions for a range of \(k = r_s/r_p\) values near 1.00, which are compared in Figure 5, and 10 000 JKTEBOP Monte Carlo simulations in each band; see Figure 6 for details. The adopted photometric elements listed in Table 6 are the weighted mean values of the EBOP solutions adopting the linear limb darkening coefficients by Van Hamme (1993). The final radiative parameters were derived from a solution that uses the weighted average of the geometric properties. Errors are based on the Monte Carlo simulations and comparison between the V and I solutions. We find that at phase 0.0, about 80% of the V light from the primary component is eclipsed, and at phase 0.5 about 85% of the V light of the secondary is blocked out.

4. PHYSICAL PARAMETERS FOR V 12

Absolute dimensions for the components of V 12 were calculated from the spectroscopic and photometric elements given in Tables 2 and 6. As seen in Table 7, masses and radii for the only slightly different components have been determined to an accuracy of about 0.6% and 1.4%, respectively. Individual V and I magnitudes are included, as calculated from the combined magnitudes outside eclipses (Section 3.1) and the luminosity ratios (Table 6). For interstellar reddening and absorption corrections, we have used \(E(B-V) = 0.087 \pm 0.010, E(V-I) = 1.31 \times E(B-V) = 0.114,\) and \(A_V = 3.1 \times E(B-V) = 0.27.\) For \(I_c (8140 \text{ Å}),\) the relations by Cardelli et al. (1989) give the same \(E(V-I)/E(B-V)\) ratio, and for the color of V 12, the \(E(V-I)/E(B-V)\) relation by Dean et al. (1978) leads to the same \((V-I)\) reddening.

4.1. The Systemic and Component Effective Temperatures

Effective temperatures \(T_{\text{eff}}\) were derived from the recent calibrations by Alonso et al. (1996), Castelli (1999), VandenBerg & Clem (2003), Ramirez & Meléndez (2005), Masana et al. (2006), and Casagrande et al. (2006). Because the surface fluxes of the components are nearly identical, the two stars have almost the same \(T_{\text{eff}}\); the empirical visual flux calibration by Popper (1980) with bolometric corrections by Flower (1996) yield a difference of only 25 K. We have therefore applied all available color indices for the combined light from Section 3.1, Stetson et al. (2004), and from 2MASS\textsuperscript{11} JHK\textsubscript{c} photometry (Cutri et al. 2003),
and the individual \((V - I)_0\) indices listed in Table 7. Results from the combined indices are presented in Table 8. For each color index, the temperatures derived from the different calibrations agree quite well. Differences in the derived temperatures between indices is, in part, due to uncertainties of the indices, which cause changes of 50–100 K, except for \(~250\) K in \((R - I)\). The temperatures based on \((V - R)\) and \((R - I)\) would increase by about 120 K and decrease by about 200 K, respectively, if the possible zero-point error in \(R\) of \(0.02\) (noted by Stetson et al. 2004) is applied. A somewhat better agreement between the temperatures is then obtained from the different indices.

For \([\text{Fe}/\text{H}] = 0.00\), the individual \((V - I)_0\) indices listed in Table 7 give temperatures of 5818 K and 5750 K (Ramírez & Meléndez 2005), 5928 K and 5858 K (VandenBerg & Clem 2003), and 5829 K and 5765 K (Casagrande et al. 2006) for the primary and secondary components, respectively. Formally we obtain temperature differences between the components higher than 25 K, as derived from the \(V\) surface flux ratio, but the

Figure 5. EBOP solutions for V12 for a range of fixed \(k\) values. Linear limb-darkening coefficients by Van Hamme (1993) were adopted. The upper left panel shows rms errors of the fit to the observations. Symbols are: cross \(V\); square \(I\).

Figure 6. Best-fitting parameter values for the 10,000 synthetic V12 I light curves created for the Monte Carlo analysis. Linear limb darkening coefficients by Van Hamme (1993) were adopted.
VandenBerg & Clem (2003), we assign 5900 K and 5875 K to the primary and secondary components, respectively, both with fixed surface gravities (log \(\text{g}\)) of 4.174 \pm 0.012 for the primary and 4.196 \pm 0.013 for the secondary component.

The best matches (highest cross-correlation peak heights) for fixed surface gravities (log \(g\)) of 4.174 and 4.191 were obtained for temperatures of 5900 K and 6000 K, metallicities of –0.14 and –0.13, and rotation velocities of 15 km s\(^{-1}\) and 17 km s\(^{-1}\), respectively, for the V12 A and B components.

**Table 6**

| Element | Value | Value |
|---------|-------|-------|
| \(i\)   | 88.62 \pm 0.05 | 80.74 \pm 0.05 |
| \(\tau_p\) | 0.0749 \pm 0.0010 | 0.0701 \pm 0.0010 |
| \(r_v\) | 0.981 \pm 15 | 0.996 \pm 14 |
| \(L_v/L_p\) | 0.913 \pm 36 | 0.927 \pm 50 |

**Table 7**

| Parameter | Primary | Secondary |
|-----------|---------|-----------|
| Absolute dimensions | | |
| \(M/M_\odot\) | 1.103 \pm 0.007 | 1.081 \pm 0.007 |
| \(R/R_\odot\) | 1.424 \pm 0.019 | 1.373 \pm 0.019 |
| \(\log g\) (cgs) | 4.174 \pm 0.012 | 4.196 \pm 0.013 |
| Photometric data | | |
| \(V\) | 15.449 \pm 0.021 | 15.548 \pm 0.023 |
| \(V_0\) | 15.180 \pm 0.037 | 15.278 \pm 0.039 |
| \(I\) | 14.663 \pm 0.030 | 14.746 \pm 0.032 |
| \((V-I)\) | 0.786 \pm 0.014 | 0.803 \pm 0.014 |
| \((V-I)_0\) | 0.672 \pm 0.019 | 0.689 \pm 0.019 |
| \(T_{\text{eff}}\) | 5900 \pm 100 | 5875 \pm 100 |
| \(M_\text{bol}\) | 3.88 \pm 0.08 | 3.98 \pm 0.08 |
| \(\log L/L_\odot\) | 0.34 \pm 0.03 | 0.30 \pm 0.03 |
| \(B.C.\) | –0.06 | –0.06 |
| \(M_V\) | 3.94 \pm 0.08 | 4.04 \pm 0.08 |
| \((m-M)_V\) | 11.507 \pm 0.085 | 11.504 \pm 0.086 |
| \(V_0 - M_V\) | 11.237 \pm 0.090 | 11.235 \pm 0.091 |
| Distance (pc) | 1768 \pm 74 | 1766 \pm 74 |

**Notes.** We have assumed \(T_{\text{eff}} = 5780\) K, \(B.C.\) = –0.08, and \(M_\text{bol}\) = 4.74. We have adopted \(E(B-V) = 0.087 \pm 0.010\), \(E(V-I) = 1.31 \times E(B-V)\), and \(A_V = 3.1 \times E(B-V)\).

uncertainties of the indices, the reddening, the metal abundance, and the calibrations themselves add up (in quadrature) to individual temperature uncertainties of about \(\pm 100\) K. Using \([\text{Fe/H}] = –0.1\) typically decreases the temperatures by less than 100 degrees. Giving higher weight to the calibration by VandenBerg & Clem (2003), we assign 5900 K and 5875 K to the primary and secondary components, respectively, both with uncertainties of \(\pm 100\) K.

4.2. Analysis of Disentangled Spectra

Analysis of the disentangled spectra was performed to provide independent values for the temperatures, metallicities, and rotational velocities of the components. We cross-correlated the disentangled spectra of each binary component against a grid of synthetic spectra\(^{12}\) spanning appropriate ranges in effective temperature, surface gravity, metallicity, and rotation velocity. The best matches (highest cross-correlation peak heights) for fixed surface gravities (log \(g\)) of 4.17 and 4.19 were obtained for temperatures of 5900 K and 6000 K, metallicities of –0.14 and –0.13, and rotation velocities of 15 km s\(^{-1}\) and 17 km s\(^{-1}\), respectively, for the V12 A and B components.

The same analysis was performed for 5 twilight sky spectra from WIYN/Hydra, resulting in a mean temperature 60 K above solar, a mean metallicity 0.06 below solar, and a mean rotational velocity 3.5 km s\(^{-1}\) above solar. We estimate that the uncertainties on temperatures and metallicities derived from WIYN/Hydra spectra from this technique are at least 150 K and 0.1 dex. Thus considering the systematic offsets for the Sun, the spectral analysis of V 12 gives results that are entirely consistent with the results from the photometric analysis. Furthermore, the rotational velocities of the binary components are consistent with the synchronous rotation (11 km s\(^{-1}\)) expected in an old circularized binary system.

4.3. The Distance and Age of V 12

The accurate masses and radii determined for the components of V 12 are independent of distance, reddening, and color-temperature transformations, and allow direct comparison with stellar models. From the absolute dimensions of the components, we determine identical distance moduli of \(5.09 \pm 0.07\) and \(5.35 \pm 0.07\), respectively, for \(M_V = 11.022 \pm 0.021\), and adopting \(E(B-V) = 0.087\), and adopting \(E(B-V) = 0.087\), model and adopting also \(E(B-V) = 0.087\), Michaud et al. (2004) get \((m-M)_V = 11.040\) from models of solar metallicity.

To determine the age of V12, we have chosen to use the recent Yongse–Yale \((Y^2)\) models by Demarque et al. (2004) and the latest Victoria–Regina (VRSS) models for scaled solar abundances for the heavy elements (VandenBerg et al. 2006). Comparisons were done for \([\text{Fe/H}] = 0.00\) \((\text{Y}, \text{Z}) = (0.266, 0.018)\) and \([\text{Fe/H}] = –0.10\) \((\text{Y}, \text{Z}) = (0.259, 0.014)\), corresponding to the range of recent values for the cluster metallicity. The two sets of models treat convective core overshooting differently, but at the age of NGC 188 overshooting is not required to match the turnoff region where V12 is located. We refer the reader to the original papers or Clausen et al. (2008) for more details on the models and their input physics.

Figure 7 shows the mass–radius diagrams with the locations of the V12 components and the \(Y^2\) and VRSS isochrones for...
relevant ages and [Fe/H] of 0.0 and −0.1. Grids of isochrones with 0.1 Gyr age separations were computed for both models using the available interpolation routines. For [Fe/H] = 0.00, the 6.4 Gyr isochrones from both models, provide the best fit to the V 12 components. For [Fe/H] = −0.1, the best-fit VRSS isochrone has an age of 6.0 Gyr, and the best-fit Y^2 isochrone has an age of 5.9 Gyr. Table 9 lists the isochrone ages for the two different models and the two different chemical compositions considered. We adopt an age of 6.2 ± 0.2 Gyr for V 12 and NGC 188. Thus, for solar metallicity, we agree with the age of 6.2 Gyr obtained by VandenBerg & Stetson (2004). We also confirm the age of 6.4 Gyr derived from solar metallicity diffusive models by Michaud et al. (2004) and the result by Salaris et al. (2004), which is 6.3 ± 0.8 Gyr for [Fe/H] = −0.03 ± 0.06. In contrast, VandenBerg & Stetson (2004) derive a much higher age (7.7 Gyr) than us for [Fe/H] = −0.10. Overall, the isochrone method applied to the NGC 188 CMD results in a much larger age uncertainty for V 12 than found by our direct method over the same abundance interval.

In Figure 8 we present mass–luminosity comparisons with models. On the theoretical side, the luminosity is independent of the mixing length assumed for convection; this is not the case for the radius. On the observational side, the luminosity includes uncertainties for the temperature calibration. In general, the models that best fit the components in the mass–radius plane are too luminous, with only the solar metallicity 6.4 Gyr Y^2 model marginally within the component errors. The best fit of VRSS and Y^2 models to the masses and luminosities of the binary components gives ages of 6.1 Gyr and 6.3 Gyr for [Fe/H] = 0.0, and 5.3 Gyr and 5.4 Gyr for [Fe/H] = −0.1. To reach agreement between the model ages determined from the mass–radius and mass–luminosity diagrams would require an increase in the effective temperature of the V 12 components. The necessary temperature changes are ~150 K and ~400 K for the [Fe/H] = 0.0 and [Fe/H] = −0.1 VRSS isochrones, and ~760 K for the [Fe/H] = −0.1 Y^2 isochrone. We note that the high sensitivity of luminosity to the effective temperature greatly enhances the uncertainty on the luminosity, making ages derived from the mass–luminosity diagrams less reliable.

Figure 9 presents the effective temperature versus radius diagram comparing the values of the V 12 components to those of the VRSS and Y^2 isochrones and 1.1 M_☉ mass tracks. In Figure 9(a), we show the 6.4 Gyr [Fe/H] = 0.0 and the 6.0 Gyr [Fe/H] = −0.1 VRSS isochrones as solid and dotted curves, respectively. In Figure 9(b), the 6.4 Gyr [Fe/H] = 0.0 and the 5.9 Gyr [Fe/H] = −0.1 Y^2 isochrones are plotted as solid and dotted curves, respectively. In both figures, mass tracks corresponding to 1.1 M_☉ are shown as gray solid and dashed curves for [Fe/H] = 0.0 and [Fe/H] = −0.1, respectively. For solar metallicity, the VRSS isochrone and track only marginally fit the observed quantities of the V 12 components, being slightly hotter, whereas for [Fe/H] = −0.10 both are clearly too hot, especially noting that abundance uncertainties of ±0.10 are included in the temperature errors. Similarly, the Y^2 isochrone and track for [Fe/H] = −0.10 are also too hot for a proper match to the binary components, although slightly closer in temperature than the corresponding VRSS models. The solar metallicity Y^2 6.4 Gyr isochrone and 1.1 M_☉ mass track, however, provide a very close match to the V 12 components. We also note that the point on the solar metallicity 6.4 Gyr Y^2 isochrone corresponding to the stellar mass of 1.09 M_☉ falls appropriately between the 1.103 M_☉ and 1.081 M_☉ components.

From the mass versus luminosity and effective temperature versus radius comparisons, the 6.4 Gyr solar-metallicity Y^2 model provides the best match to the observed and derived properties of the V 12 components. However, we discuss in Section 5 how a zero-point error in the I-band photometry from Stetson et al. (2004), may cause the derived temperatures for the V 12 components to be too cool by ~100–150 K. With a correction for such a temperature offset, the
5. NGC 188 AND V 12

The purpose of this section is to present V 12 in the NGC 188 CMD, and to investigate how well the VRSS and $Y^2$ isochrones that best fit the V 12 components in the mass–radius diagram, fit the rest of the cluster’s main-sequence, turn-off, and giant branch stars. We show in Figure 10 the NGC 188 V–I versus V CMD using the photometry from Stetson et al. (2004). All stars brighter than $M_V$ of 4.5 are single radial-velocity and proper-motion members of NGC 188 (Geller et al. 2008; Platais et al. 2003). Stars fainter than $M_V$ of 4.5 are proper-motion members of NGC 188 (Platais et al. 2003). The position of V 12 and of its components are marked using the V magnitudes and V–I colors listed in Table 7. Adopting the distance ($V_0 - MV = 11.624$) and ages of V 12 determined from the analysis of V 12 in Section 4.3, and a reddening of 0.087, we overplot in the left panel of Figure 10 the 6.4 Gyr solar metallicity and the 6.0 Gyr $[\text{Fe/H}] = -0.1$ VRSS isochrones. In the right panel of Figure 10 we have overplotted the 6.4 Gyr solar metallicity and the 5.9 Gyr $[\text{Fe/H}] = -0.1$ $Y^2$ isochrones. For the solar metallicity isochrones we have marked the turnoff masses nearest the V 12 primary and secondary components.

Both VRSS isochrones fit the main-sequence, turnoff, and giant branch of NGC 188 well. The $Y^2$ isochrones follow the turnoff curvature well, but both are too blue on the lower main-sequence, and the metal-poor $Y^2$ isochrone also falls to the blue of the giant branch. It is clear that without the constraints on the distance and age set by V 12, and on the cluster metallicity by spectroscopic studies, good fits to the cluster stars could be obtained from a range of different cluster metallicities, distances, and ages. For NGC 188, this is demonstrated well by Stetson et al. (2004), who show that ages between 5.9 Gyr and 8.1 Gyr result from the isochrone method when plausible ranges in metallicity and distance modulus are considered. This age-range corresponds to $\sim 33\%$ of their mean cluster age of $6.8_{-0.9}^{+1.1}$ Gyr. With V 12 we provide a constraint on the age of NGC 188 with only a $\lesssim 10\%$ uncertainty due primarily to
the uncertainty in the cluster metallicity. Judging from current spectroscopic measurements and from the best-fit isochrones to the cluster, it is likely that the cluster metallicity is between solar and $\approx -0.1$. With better determination of the cluster metallicity, the age of V12 and NGC 188 can be further improved.

We note that in the $V-I$ colors from Stetson et al. (2004), V12 and thus both its components are offset to the red by a few hundreds of a magnitude relative to cluster turnoff. The offset is likely due to a zero-point error in the $I$ band, because the Stetson et al. $B-V$ color of V12 and its components match the $B-V$ color of the cluster turnoff. Similar offsets for V12 are found in the $B-V$ and $V-I$ colors in the photometry from Sarajedini et al. (1999). Because we calibrate our photometry using the Stetson et al. (2004) photometry for V12 (see Section 3.1), we inherit this $I$ band zero-point shift. Therefore, in Figure 10, V12 and both its components display a slight red offset with respect to the cluster turnoff. The $V-I$ color offset correspond to $\approx 100$–150 K and may explain, in part, the discrepancies in luminosity and effective temperature between V12A,B and the VRSS and $Y2$ isochrones in Figures 8 and 9. The color offset has no affect on the age determination for V12 in this paper because the age is based on the stellar masses and radii only. However, any change in the color of V12 will affect the distance determined for the binary and thus NGC 188.

6. SUMMARY AND CONCLUSIONS

We have presented time-series photometric and spectroscopic observations of the detached, double-lined, eclipsing spectroscopic binary V12 in the old open cluster NGC 188. We have determined masses of $1.103 \pm 0.007 \, M_\odot$ and $1.081 \pm 0.007 \, M_\odot$, and radii of $1.424 \pm 0.019 \, R_\odot$ and $1.373 \pm 0.019 \, R_\odot$ for the binary primary and secondary components. The uncertainties in the component masses and radii are not affected by the reddening, metallicity, and the distance to the binary. From the absolute dimensions of the binary components, we derive identical distance moduli of $V_0 - M_V = 11^\circ 24 \pm 0^\circ 09$ for both components, corresponding to $1770 \pm 75$ pc.

By comparing the masses and radii of the binary components to the VRSS and the $Y^2$ model isochrones with $[\text{Fe/H}] = -0.1$ and $[\text{Fe/H}] = 0.0$, we determine a mean age of 6.2 Gyr for V12 and thus NGC 188, with an uncertainty of 0.2 Gyr. This uncertainty is primarily due to the 0.1 range in $[\text{Fe/H}]$ for NGC 188 found in the literature. Our age for V12 agrees with the age determined by VandenBerg & Stetson (2004) for a solar metallicity isochrone, and with the ages derived by Michaud et al. (2004) and Salaris et al. (2004). We find good agreement between the ages derived from both the VRSS and $Y^2$ models. The solar-metallicity 6.4 Gyr $Y^2$ isochrone matches well the masses, radii, and effective temperatures of both the primary and secondary components of V12. The corresponding VRSS isochrone has temperatures slightly hotter ($\sim 30$ K) at the component radii, but still fit the components within the errors. A systematic offset in the $V-I$ color of V12 from Stetson et al. (2004) may explain the temperature discrepancies between the V12 components and the VRSS isochrones and mass tracks. Any future correction of the $V-I$ color for V12 will change its distance.

We use the distance and ages for V12, together with best estimates for the metallicity and reddening of NGC 188, to investigate the locations of the corresponding VRSS and $Y^2$ isochrones relative to cluster members in the CMD. We find that those isochrones fit the cluster giant branch, turnoff, and upper main-sequence reasonably well. However, equally good or better fits to the cluster stars could be obtained by adopting different model metallicities, distances, and ages. This was demonstrated well in Stetson et al. (2004) where plausible changes in the model metallicity and distance result in a range of ages from 5.9 Gyr to 8.1 Gyr for NGC 188—more than 3 times that resulting from our analysis of V12.

The age of V12 and NGC 188 can be further improved from better determination of the metallicity of NGC 188 from
spectroscopic studies of main sequence, turnoff, and subgiants in NGC 188. Additional radial velocity measurements, and an effort to obtain improved light curves in more bandpasses, could also provide masses and radii with smaller errors, and thus put better constraints on the stellar models. Finally, additional precise eclipse photometry in, e.g., the $K$-band can make possible an independent determination of the distance to V12 via surface–brightness relations (e.g., di Benedetto 1998; Kervella et al. 2004).

This work has been supported by NSF grant AST-0406615 to the UW-Madison, a fellowship from the Danish Research Academy to S.M., and partial support to S.M. from the Kepler mission via NASA Cooperative Agreement NCC2-1390. The projects “Stellar structure and evolution—new challenges from ground and space observations” and “Stars: Central engines of the evolution of the Universe,” carried out at Aarhus University and Copenhagen University, are supported by the Danish National Science Research Council. F.G. gratefully acknowledges financial support from the Danish Astroidy Science Centre (DASC) at the University of Århus and from the Carlsberg Foundation. We thank observers and staff at the WIYN, Nordic Optical, Flemish Mercator, and Bialkow telescopes. We thank P. Maxted for making his TDOCCOR software available and J. Southworth for many valuable discussions and for access to is JKTEBOP code. We are grateful to E. Sturm for providing his original disentangling code, and to him and J.D. Pritchard for modifying it for use at Linux/Unix computer systems. The following Internet-based resources were used in research for this paper: the NASA Astrophysics Data System; the SIMBAD database and the VizIR service operated by CDS, Strasbourg, France; the arXiv scientific paper preprint service operated by Cornell University; This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation.

REFERENCES

Alonso, S., Arribas, S., & Martínez-Roger, C. 1996, A&A, 313, 873
Andersen, J. 1991, A&AR, 3, 91
Bonatto, C., Bica, E., & Santos, Jr., J. F. C. 2005, A&A, 433, 917
Caputo, F., Chieffi, A., Castellani, V., Collados, M., Roger, C. M., & Paez, E. 1990, AJ, 99, 261
Cardelli, J. A., Clayton, G. C., & Mathis, J. S. 1989, ApJ, 345, 245
Casagrande, L., Pinotinare, L., & Flynn, C. 2006, MNRAS, 373, 13
Castelli, F. 1999, A&A, 346, 564
Claret, A. 2000, A&A, 363, 1081
Clausen, J. V. 2004, New Astron. Rev., 48, 679
Clausen, J. V., & Gimenez, A. 1987, in 10th European Regional Astronomy Meeting of IAU, Evolution of Galaxies, ed. J. Palous (Ondrejov: Czechoslovak Academy of Sciences), 185
Clausen, J. V., et al. 2008, A&A, 487, 1095
Cutri, R. M., et al. 2003, http://www.ipac.caltech.edu/2mass/releases/allsky/doc/expsup.html
Dean, J. F., Warren, P. R., & Cousins, A. W. J. 1978, MNRAS, 183, 569
Demarque, P. R., & Larson, R. B. 1964, ApJ, 140, 544
Demarque, P., Green, E. M., & Guenther, D. B. 1992, AJ, 103, 151
Demarque, P., Woo, J.-H., Kim, Y.-C., & Yi, S. K. 2004, ApJS, 155, 667
di Benedetto, G. P. 1998, A&A, 339, 858
Dinescu, D. I., Demarque, P., Guenther, D. B., & Pinsonneault, M. H. 1995, AJ, 109, 2090
Eggen, O. J., & Sandage, A. R. 1969, ApJ, 158, 669
Etzel, P. B. 1981, in Photometric and Spectroscopic Binary Systems, ed. E. B. Corling & Z. Kopal (Dordrecht: Reidel), 111
Etzel, P. B. 2004, SBOP: Spectroscopic Binary Orbit Program (San Diego State University)
Flower, P. J. 1996, ApJ, 469, 355
Fornal, B., Tucker, D. L., Smith, J. A., Allam, S. S., Rider, C. J., & Sung, H. 2007, AJ, 133, 1409
Friel, E. D., & Janes, K. A. 1993, A&A, 267, 75
Friel, E. D., et al. 2002, AJ, 124, 2693
Geller, A. M., Mathieu, R. D., Harris, H. C., & McClure, R. D. 2008, AJ, 135, 2264
Giménez, A., & Clausen, J. V. 1996, in ASP Conf. Ser. 90, The Origins, Evolution, and Destinies of Binary Stars in Clusters, ed. J.-C. Mermilliod & E. F. Milone (San Francisco, CA: ASP), 44
Grundahl, F., Clausen, J. V., Hardis, S., & Frandsen, S. 2008, A&A, 492, 171
Guinan, E. F., et al. 1998, ApJ, 509, 212
Hobbs, L. M., Thorburn, J. A., & Rodriguez-Bell, T. 1990, AJ, 100, 710
Hynes, R. I., & Maxted, P. F. L. 1998, A&A, 331, 167
Iben, I. J. 1967, Science, 155, 785
Kaluzny, J., Pych, W., Rucinski, S. M., & Thompson, I. B. 2006, Acta Astron., 58, 263
Kaye, V. A. W., & Landolt, A. U. 1999, AJ, 128, 287
Kupka, F., Piskunov, N., Ryabchikova, T. A., Stempels, H. C., & Weiss, W. 1999, A&AS, 138, 119
Kurucz, R. L. 1993, in Light Curve Modelling of Eclipsing Binary Stars, ed. E. F. Milone (Berlin: Springer), 93
Kwee, K. K., & van Woerden, H. 1956, Bull. Astron. Inst. Netherlands, 12, 327
López-Morales, M., & Shaw, J. S. 2007, PASP, 126, 26
Meynet, G., Mermilliod, J.-C., & Maeder, A. 1993, A&AS, 98, 477
Michaud, G., Richard, O., & Richer, J. H. 1990, ApJ, 360, 642
Nelson, B., & Davis, W. D. 2003, AJ, 126, 2922
Platais, I., Kozhurina-Platais, V., Mathieu, R. D., & Van Altena, W. F. 2003, AJ, 126, 2922
Popova, M., & Kraicheva, Z. 1984, Astron. Astrophys. Lett., 18, 64
Popper, D. M. 1980, ARA&A, 18, 115
Popper, D. M., & Etzel, P. B. 1981, AJ, 86, 102
