We present the distributions of the geometrical covering factors of the dusty tori (\(f_2\)) of active galactic nuclei (AGNs) using an X-ray selected complete sample of 227 AGNs drawn from the Bright Ultra-hard XMM-Newton Survey. The AGNs have \(z\) from 0.05 to 1.7, 2–10 keV luminosities between \(10^{42}\) and \(10^{46}\) erg s\(^{-1}\), and Compton-thin X-ray absorption. Employing data from UKIDSS, 2MASS, and the Wide-field Infrared Survey Explorer in a previous work, we determined the rest-frame 1–20 \(\mu\)m continuum emission from the torus, which we model here with the clumpy torus models of Nenkova et al. Optically classified type 1 and type 2 AGNs are intrinsically different, with type 2 AGNs having, on average, tori with higher \(f_2\) than type 1 AGNs. Nevertheless, \(\sim20\%\) of type 1 AGNs have tori with large covering factors, while \(\sim23\%–28\%\) of type 2 AGNs have tori with small covering factors. Low \(f_2\) are preferred at high AGN luminosities, as postulated by simple receding torus models, although for type 2 AGNs the effect is certainly small. \(f_2\) increases with the X-ray column density, which implies that dust extinction and X-ray absorption take place in material that share an overall geometry and most likely belong to the same structure, the putative torus. Based on our results, the viewing angle, AGN luminosity, and also \(f_2\) determine the optical appearance of an AGN and control the shape of the rest-frame \(\sim1–20\ \mu\)m nuclear continuum emission. Thus, the torus geometrical covering factor is a key ingredient of unification schemes.

Key words: galaxies: active – galaxies: nuclei – infrared: galaxies – quasars: general
framework of “clumpy unification” type 2 AGNs should have tori with geometrical covering factors higher, on average, than type 1 AGNs (for a recent review on this topic see Elitzur 2012). Recent analyses of the nuclear infrared emission of AGNs with radiative transfer models of clumpy tori indicate that this might indeed be the case (Ramos Almeida et al. 2011; Ichikawa et al. 2015). Unfortunately, until very recently such studies have been restricted to small samples of mostly nearby Seyfert galaxies and quasars (Mor et al. 2009; Nikutta et al. 2009; Ramos Almeida et al. 2009, 2011; Alonso-Herrero et al. 2011; Deo et al. 2011; Lira et al. 2013).

Thanks to the advent of the all-sky infrared survey conducted with the Wide Field Infrared Survey Explorer at 3.4, 4.6, 12, and 22 μm (WISE; Wright et al. 2010) it is now possible to constrain the properties of the AGN tori, in particular its geometrical covering factor, in large, representative samples of objects spanning a broad range of both redshifts and AGN luminosities. The aim of this study is to verify observationally the validity of unified schemes in the framework of clumpy torus models. To do so we have determined, for the first time, the distribution of covering factors of AGN tori using a large, uniformly selected, complete sample of AGNs. We have investigated whether type 1 and type 2 AGNs are indeed intrinsically different objects, as recently claimed in the literature, by comparing the distributions of covering factors of their tori. Finally we have determined the dependence (or lack of) of the torus covering factor on the line of sight absorption measured in X-rays and the AGN luminosity.

The 227 AGNs used in this study are drawn from the Bright Ultra-hard XMM-Newton Survey (BUXS). BUXS is a complete flux-limited sample of 255 X-ray bright AGNs (\(L_{2-10\text{keV}} > 6 \times 10^{44} \text{erg s}^{-1} \text{cm}^{-2}\)) detected at 4.5 to 10 keV energies with the XMM-Newton European Photon Imaging Camera (EPIC)-pn (Strüder et al. 2001). The objects were selected at such high energies to reduce biases against highly absorbed AGNs as much as possible. The survey covers 44.43 deg\(^2\) of the northern sky (galactic latitudes \(|b| > 20^\circ\)) distributed over 381 XMM-Newton observations with good quality for serendipitous source detection (Mateos et al. 2008, 2012). For complete details on the survey design, sample selections and UV/optical spectroscopic identification and classification of the objects, see Mateos et al. (2012, 2015). At the time of writing the identification completeness is 98.4% (251 objects). Such a high identification rate guarantees that our study will not suffer from biases associated with optical identification incompleteness, which are more severe for highly obscured type 2 AGNs.

We have good-quality XMM-Newton spectra for all BUXS sources, which constrain directly both the line of sight rest-frame absorbing column densities and X-ray luminosities (see M15). Throughout this paper \(L_X\) represents intrinsic, absorption-corrected luminosities in the rest-frame 2–10 keV band.

For the analysis presented here we selected the 233 non-blazar AGNs with \(L_X > 10^{42}\) and \(z < 1.7\). The luminosity cut was applied to reduce to a minimum the uncertainties associated with the determination of the infrared emission of the tori of our objects by increasing the contrast of the AGNs over the underlying emission from the AGN hosts (12 objects removed; see Section 3.1). The redshift cut was imposed to assure adequate wavelength sampling of the torus rest-frame continuum emission (six objects removed). Finally, we excluded five type 1 AGNs and one type 2 AGN without detections with signal-to-noise-ratios (\(S/N\)) \(> 2\) at all 3.4, 4.6, and 12 μm in the final data release of WISE (AllWISE; Cutri et al. 2013). As the number of objects not detected with WISE above our selection threshold is rather small, and in addition, these objects span a broad range of \(L_X\) and \(z\), removing them from the sample should not bias our results. All the above selection criteria left us with a sample of 227 AGNs with \(L_X\) from \(10^{42}\) to \(10^{46} \text{erg s}^{-1}\) and \(0.05 < z < 1.7\).

We classified our AGNs as type 1 if permitted and semi-forbidden broad emission lines (line velocity widths \(>1500 \text{km s}^{-1}\)) were detected in their rest-frame UV/optical spectra (132 objects) and as type 2 if they showed narrow
emission lines only (line velocity widths <1500 km s\(^{-1}\); 75 objects) or had a galaxy-like spectrum with no emission lines (3 objects). Due to the controversy regarding the nature of intermediate Seyfert types 1.8 and 1.9 as type 1 or type 2 AGN we kept such objects as a separate class (17 objects).\(^6\)

3. METHODOLOGY

3.1. Isolating the Torus Emission

In M15 we determined infrared SEDs associated with the emission from the dusty torus for the AGNs in BUXS. To do so we conducted a thorough analysis of the rest-frame UV-to-infrared photometric SEDs to correct the cataloged infrared fluxes for any contamination associated with both the host galaxies and the direct emission from the AGN accretion disk. Our SEDs are based on data from the Sloan Digital Sky Survey (SDSS; Abazajian et al. 2009), the Two Micron All Sky Survey (2MASS; Jarrett et al. 2000; Cutri et al. 2003), the UKIRT Infrared Deep Sky Survey (UKIDSS; Lawrence et al. 2007), and WISE (Wright et al. 2010). To decompose the observed fluxes into AGN and galaxy emission we used the SED fitting tool SED Analysis using BayesStatian Statistics (SEABAS,\(^8\) Rovilos et al. 2014).

Very briefly, to model the emission from the accretion disk we used the type 1 quasar SED from Richards et al. (2006) at rest-frame wavelengths \(\lambda < 0.7 \mu m\) and a power-law \(\lambda f_\lambda \propto \lambda^{-1}\) at longer wavelengths. To redden the accretion disk we used the Gordon & Clayton (1998) Small Magellanic Cloud extinction law at \(\lambda < 0.33 \mu m\) and the Cardelli et al. (1989) Galactic extinction law at \(\lambda > 0.33 \mu m\). In both cases we assumed \(R_V = 3.1\). To characterize the continuum emission from the AGN dusty torus we used the Seyfert 1 and the two Seyfert 2 templates corresponding to rest-frame X-ray absorbing column densities \(N_H < 10^{24} \text{ cm}^{-2}\) from Silva et al. (2004). Finally, to reproduce the emission from the stellar population of the AGN hosts at rest-frame optical-near-infrared wavelengths we used a library of 75 stellar templates from Bruzual & Charlot (2003). The templates have solar metallicity and a Chabrier initial mass function (Chabrier 2003) and were generated using 10 exponentially decaying star formation histories with characteristic times \(\tau = 0.1-30\) Gyr and a model with constant star formation, and a set of ages in the range 0.1–13 Gyr. To redden the stellar templates we used the Calzetti et al. (2000) dust extinction law. An example of the SED decomposition analysis is illustrated in Figure 1. It is important to highlight that we have adopted the same templates and SED decomposition procedure to isolate the AGN torus emission of all sample objects.

In M15 we demonstrated that stellar contamination of cataloged fluxes in the infrared regime at rest-frame wavelengths shorter than \(\sim 6 \mu m\) is significant, especially for type 2 objects. Only for type 1 objects with \(L_X > 10^{43} \text{ erg s}^{-1}\) do the AGNs outshine the host galaxy in the infrared band. The tight correlation found between rest-frame 6 \(\mu m\) luminosities, corrected for contamination from the accretion disk and AGN hosts, and 2–10 keV intrinsic (absorption-corrected) luminosities, supports the hypothesis that the infrared SEDs determined from our decomposition analysis are associated with dust heated by the intense radiation field of the AGN. This dust is most likely located in the putative torus on parsec scales. Hereafter, nuclear infrared SEDs will refer to the emission from the torus.

We focus our analysis here on rest-frame wavelengths longer than 1 \(\mu m\) since this is the spectral region where the AGN torus emits the bulk of its radiation. Although in M15 we demonstrate that, at the luminosities of our AGNs, contamination due to star formation at these wavelengths should be negligible, to minimize such effects we have treated the WISE 22 \(\mu m\) fluxes of all 12 objects with \(L_X < 5 \times 10^{42} \text{ erg s}^{-1}\) (five type 1 AGNs, six type 2 AGNs, and one Sy1.9), whether detected or not at these wavelengths, as upper limits. Nevertheless, we have checked that this assumption does not affect our main results.

3.2. SED Fitting with CLUMPY Models

To describe the nuclear infrared emission of our objects we have used the radiative transfer models by N08. In these models the material obscuring the AGN nuclear region is treated as a medium with a toroidal shape, where the dust and gas are distributed in high-density clumps inside it. The angular distribution of clouds has no sharp cutoff boundary and is described as a Gaussian of width \(\sigma\),

\[
N_T(\beta) = N_0 e^{-(\beta^2/\sigma^2)},
\]

where \(N_T\) is the line of sight number of clouds, \(\beta = \pi/2 - i\) is the inclination angle of the torus equatorial plane with respect to the line of sight and \(i\) is the viewing angle from the torus axis. \(N_0\) represents the mean number of clouds along radial equatorial rays. In the N08 models the radial distribution of clouds is parameterized as a power law, \(N(r) \propto r^{-q}\), where \(N\) is the number of clouds and \(q\) is the power-law index. The torus radial thickness \((Y)\) is defined as the ratio of the outer \((R_o)\) to inner \((R_d)\) radius of the distribution of clouds, where \(R_d\) is set by the AGN luminosity and the dust sublimation temperature

\(^6\) Objects of intermediate Seyfert type 1.9 can be identified up to \(z = 0.2-0.4\), depending on whether or not the H\(\alpha\) emission line is outside the observable wavelength range of our spectroscopic data.

\(^8\) http://astro.dur.ac.uk/~erovilos/SEABASs/
 Mean number of clouds along equatorial rays
 Torus radial thickness
 Single cloud optical depth
 Torus angular width
 Index of the radial distribution of clouds

9 http:

fraction of the sky obscuring the AGN nuclear region,

\( f_2 = 1 - \int_0^{\pi/2} P_{\text{esc}}(\beta) \cos(\beta) d\beta, \)

(3)

where \( P_{\text{esc}} \) is integrated over all angles (Mor et al. 2009). As \( f_2 \) is independent of the inclination angle, it represents the true intrinsic fraction of optically obscured type 2 objects in the entire AGN population.

Figure 2 shows three examples of the typical nuclear infrared SEDs used in our study and the SED fitting results obtained with BayesCLUMPY. The insets show the normalized posterior distributions of \( f_2 \) derived from the fits. To obtain the distribution of \( f_2 \) for a sample of objects fully taking into account the uncertainties from the fits we first concatenated together the individual arrays of values of \( f_2 \) returned from the MCMC analysis for each object and then we computed the probability distribution of the combined array of values of \( f_2 \).

To compare different distributions of \( f_2 \) we have used the two-sample Kolmogorov–Smirnov (KS) test and Monte Carlo simulations to determine the probability of rejecting the null hypothesis that the two samples are drawn from the same parent population. Each time we ran our simulations we used bootstrap to randomly select 10^5 times the sample objects used to determine the distributions of \( f_2 \).

For illustration purposes, throughout this paper we have used a bin size of 0.03 to represent the distributions of \( f_2 \), but we stress that all computations are based on the arrays of values of \( f_2 \). All distributions are normalized to have an area of one under the curve.

4. RESULTS

As indicated before, we have used the N08 models to reproduce the nuclear infrared emission associated with the dusty tori of AGN and to determine their dust covering factors. Therefore, the results inferred from our SED fits should be considered in the framework of these models.

4.1. \( f_2 \) versus Optical Class

Figure 3 shows the distribution of \( f_2 \) for our full sample of AGNs. It is evident that type 1 and type 2 AGNs have significantly different distributions of \( f_2 \), in the sense that type 2 AGNs overall have tori with higher covering factors than type 1 AGNs. Based on the KS test and our simulation analysis we can reject the null hypothesis that the two samples are drawn from the same parent population with a confidence level higher than 99.99%. Nevertheless, we find that there is a large overlap between the distributions of \( f_2 \) for type 1 and type 2 AGNs, in good agreement with previous studies based on high-spatial resolution nuclear infrared photometric data and/or mid-infrared spectroscopic data for small samples of local Seyferts and PG quasars (e.g., Mor et al. 2009; Ramos Almeida et al. 2009, 2011; Alonso-Herrero et al. 2011; Ichikawa et al. 2015).

The distributions of \( f_2 \) that we find for the two AGN populations are significantly broader than claimed in the above studies. As we will see in the following sections, such apparent discrepancies are not associated with higher uncertainties in our

\[ f_2 = 1 - \int_0^{\pi/2} P_{\text{esc}}(\beta) \cos(\beta) d\beta, \]

9 While we believe that the methodology applied is reliable, a more coherent way to infer the global distribution of the covering factor would have been to use a hierarchical Bayesian model. Nevertheless, such an approach would have entailed the typical shrinkage of hierarchical modeling.
analysis compared to previous studies but to type 1 (type 2) AGNs having rather large (small) torus covering factors. Since such objects are rare, sampling them requires studies of large and complete samples of AGNs, such as ours. For example, as we will see in Section 4.4.1, if we use $f_2 = 0.5$ as a threshold to separate AGN tori with low and high covering factors, we find that 26 out of 132 type 1 AGNs have tori with high covering factors, while 22 out of 78 type 2 AGNs have tori with low covering factors.

As indicated before, we stress that we have used the same SED decomposition procedure to isolate the AGN torus emission of all sample objects. Our SED fits with BayesCLUMPY take into account both the quality of the cataloged infrared photometric data, which is similar among our type 1 and type 2 AGNs, and the uncertainties from the SED decomposition analysis. We have also checked that the distributions of $f_2$ for type 1 AGN have widths, based on the 16th and 84th percentiles, that are indistinguishable from those of type 2 AGN. All this guarantees that any differences in the torus properties among AGNs with different optical spectroscopic classifications reported here are genuine and not an artifact of either the SED decomposition analysis or the quality of the infrared data.

Interestingly, we find that AGNs classified as Sy1.8–1.9 have a rather flat distribution of $f_2$ that is significantly different from those of type 1 and type 2 AGNs. Thus, from the infrared point of view, we find that it is highly unlikely that all Sy 1.8–1.9 are simply ordinary type 1 AGNs caught in a low flux state during the UV/optical spectroscopic observations, as significant differences exist between the properties of the tori of these two AGN classes. A KS test returns probabilities of 99.78% and 97.98% for rejecting the null hypothesis that the distributions of $f_2$ for Sy 1.8–1.9 and those obtained for type 1 and type 2 AGN are identical. Therefore, alternative processes must play a role. For example, our finding that 12 out of the 17 intermediate-type objects are absorbed in X-rays (see Section 4.2) favors a scenario where most of our Sy1.8–1.9 objects have broad-line regions reddened by optically thin dust located either in the torus or on physical scales of the narrow-line region or the host galaxies (e.g., Alonso-Herrero et al. 2011).

We note that, if some high-$z$ Sy1.8–1.9 objects are still present in our sample of type 2 AGNs, the effect would be to reduce the differences between the $f_2$ distributions of type 1 and
type 2 AGNs. Clearly, this would not change our results since we have already found that we can reject the hypothesis that the distributions of $f_2$ for type 1 and type 2 AGNs are drawn from the same parent population with a confidence level higher than 99.99%.

Finally, we have used the results from our SED decomposition analysis to compare the distributions of $f_2$ for all objects with detected UV/optical broad emission lines (132 type 1 AGN and 17 Sy1.8–1.9s) with low and high extinction toward their accretion disk. To separate the objects we have used an extinction of $E(B-V) = 0.32$, or $A_V = 1$ mag assuming a Galactic standard conversion. Such a value has often been used in the literature to identify moderately reddened type 1 AGNs (e.g., Urrutia et al. 2012; Lacy et al. 2013 and references therein). Based on the chosen extinction threshold, 13 out of 132 type 1 AGNs and 10 out of 17 Sy1.8–1.9s are classified as moderately reddened objects ($E(B-V)$ in the range 0.32–0.65; see M15 for details). We find that, as expected, higher $f_2$ are preferred in reddened broad-line AGN. According to the KS test we can reject the null hypothesis that the $f_2$ distributions of the two samples (reddened and unreddened broad-line AGNs) are drawn from the same parent population with a 99.3% confidence level.

Based on the results presented in this section we can conclude that, type 1, type 2, and probably also intermediate-type AGNs are on average intrinsically different, as has been previously reported in the literature (e.g., Ramos Almeida et al. 2011).

4.2. $f_2$ versus X-Ray Absorption

The discovery that the UV/optical spectroscopic classifications of AGNs correlate well with the absorption properties measured in X-rays has provided strong observational evidence favoring standard orientation-based unified models. Nevertheless, it is well known that AGNs exhibit a large range of dust-to-gas ratios and that for a non-negligible fraction of objects, gas absorption in X-rays and dust extinction in the UV-to-infrared spectral band are not always detected together (e.g., Maiolino et al. 2003; Mateos et al. 2005a, 2005b, 2010; Tozzi et al. 2006; Garret et al. 2007; Winter et al. 2009; Corral et al. 2011; Page et al. 2011; Scott et al. 2011; González-Martín et al. 2014; Merloni et al. 2014).

To investigate whether a physical or geometrical connection exists between the material responsible for the X-ray absorption and UV-to-infrared obscuration, we have computed the distributions of $f_2$ for AGNs with different levels of X-ray absorption. To have a good representation of both type 1 and type 2 AGNs across the full range of measured X-ray column densities, we have divided the sample in four different bins: $N_H < 4 \times 10^{21}$ cm$^{-2}$ (henceforth X-ray unabsorbed), $4 \times 10^{21} < N_H < 10^{23}$ cm$^{-2}$, $10^{23} < N_H < 4 \times 10^{23}$ cm$^{-2}$ and $4 \times 10^{23} < N_H < 1.4 \times 10^{24}$ cm$^{-2}$. Figure 4 summarizes the results of this analysis. Although in Figure 4 we show the distributions of $f_2$ for objects classified as Sy1.8–1.9 for completeness, we do not use them in the analysis presented in this section, as we are clearly limited by small number statistics. Nevertheless, our results suggest that the distribution of $f_2$ is rather flat for both X-ray unabsorbed and absorbed Sy1.8–1.9s.

We note that none of our X-ray selected sources have a best-fit X-ray column density in the Compton-thick regime. Nevertheless, considering the uncertainties in $N_H$, we cannot rule out unambiguously Compton-thick absorption in five type 2 AGNs (all five sources belong to the $4 \times 10^{22} < N_H < 1.4 \times 10^{23}$ cm$^{-2}$ bin). As an independent test, we have determined the $L_X^{obs} / L_6$ luminosity ratio for these objects where $L_X^{obs}$ are observed (i.e., not corrected for intrinsic absorption) rest-frame 2–10 keV luminosities and $L_6$ are the monochromatic luminosities of the torus emission at rest-frame 6 μm. The later have been shown to be a good proxy for the AGN intrinsic power (Lutz et al. 2004; Ramos Almeida et al. 2007; Fiore et al. 2009; Georgantopoulos et al. 2011; Mateos et al. 2015; Stern 2015). Based on the relationship between $L_X$ and $L_6$ from M15 we find that, in all five cases, the $L_X^{obs} / L_6$ ratio is consistent with Compton-thin absorption. Finally, we have used a column density of $4 \times 10^{21}$ cm$^{-2}$ to separate unabsorbed and absorbed AGNs. Assuming a Galactic standard dust-to-gas ratio, an $N_H$ of $4 \times 10^{23}$ cm$^{-2}$ corresponds to $A_V \sim 2$ mag, or $E(B-V) \sim 0.65$, the extinction level that separates optical type 1 from type 2 AGNs (Caccianiga et al. 2008; Merloni et al. 2014).

Interestingly we find that, type 1 and type 2 AGNs with similar levels of X-ray absorption have significantly different distributions of torus geometrical covering factors. This result also holds for X-ray unabsorbed objects (Figure 4 top left). We can reject the null hypothesis that the distributions of $f_2$ for X-ray unabsorbed type 1 and type 2 AGNs are drawn from the same parent population with a confidence higher that 99.99%. Clearly, intrinsic differences exist among the torus properties of these two groups of objects. Thus, although the host galaxies could totally outshine the AGN emission in the optical band in some objects (e.g., Moran et al. 2002; Severgnini et al. 2003; Page et al. 2006), this cannot be the sole factor for determining the optical appearance of X-ray unabsorbed type 2 objects (Panessa & Bassani 2002; Bianchi et al. 2008, 2012; Panessa et al. 2009; Gallo et al. 2013). Indeed only 4 out of 10 X-ray unabsorbed type 2 AGNs in our sample have $L_X < 10^{33}$ erg s$^{-1}$, where host galaxy dilution can be an important effect (Caccianiga et al. 2007).

The distributions of $f_2$ for X-ray unabsorbed type 1 and type 2 AGNs (Figure 4 top left) are largely indistinguishable from those of absorbed AGNs with $N_H$ in the range $4 \times 10^{22} < N_H < 10^{23}$ cm$^{-2}$ (Figure 4 top right). This suggests that, up to column densities of $\sim 10^{23}$ cm$^{-2}$, there is no significant correlation between $f_2$ and $N_H$. Nevertheless, at $N_H < 10^{23}$ cm$^{-2}$ gas and dust in the AGN hosts might be contaminating some of our measurements, especially for type 2 AGNs (e.g., Alonso-Herrero et al. 2003; Guainazzi et al. 2005; Goulding et al. 2012). Therefore we focus our attention on objects with column densities $N_H > 10^{23}$ cm$^{-2}$, as such high column densities should be associated with the torus.11 As we only have three type 1 objects with $N_H > 10^{23}$ cm$^{-2}$ in BUX the distribution of $f_2$ for such objects may not be representative of the overall population of highly absorbed type 1 AGNs. Thus, in what follows we restrict our discussion to type 2 objects. Nevertheless, we note that, based on the KS test and our simulation analysis, we cannot reject the null hypothesis that type 1 and type 2 AGNs are drawn from the same parent population with a confidence higher that 99.99%.
hypothesis that the distributions of $f_2$ for unabsorbed, mildly absorbed ($4 \times 10^{23} \text{ cm}^{-2} < N_H < 10^{23} \text{ cm}^{-2}$), and highly absorbed ($10^{23} \text{ cm}^{-2} < N_H < 4 \times 10^{23} \text{ cm}^{-2}$) type 1 AGNs are drawn from the same parent population. We find that the covering factor of a typical type 2 AGN torus increases with $N_H$ (Figure 4 bottom plots). This effect becomes more pronounced at column densities approaching the Compton-thick regime.

Our analysis demonstrates that, not only do AGNs with different optical classifications have, on average, tori with different covering factors, but also the most highly absorbed type 2 AGNs have the highest covering factors of nuclear dust. Since all sources with absorbing column densities $N_H > 4 \times 10^{23} \text{ cm}^{-2}$ have remarkably similar distributions of $f_2$ it is highly unlikely that statistical fluctuations associated with the small sample size affect our results. Such, high dust covering factors seem to be a common property of the most absorbed Compton-thin type 2 AGNs (but see also Silva et al. 2004).

Interestingly, Ricci et al. (2011) found that type 2 AGNs with column densities in the range $10^{23} \text{ cm}^{-2} \leq N_H < 10^{24} \text{ cm}^{-2}$ have a stronger X-ray reflection component than both type 1 and type 2 AGNs with $N_H < 10^{23} \text{ cm}^{-2}$. If the material in the torus is the main X-ray reflector, these results are consistent with a scenario where the covering factor of the torus is higher in the most highly absorbed Compton-thin type 2 AGNs. This is supported by our findings.

X-ray spectral variability studies have shown that a large fraction of the X-ray absorbing cold gas must be located at the physical scales of the broad-line region, probably in dust-free clouds in the innermost part of the torus, inside the dust sublimation radius (e.g., Elitzur 2008; Risaliti et al. 2009, 2011; Bianchi et al. 2012; Markowitz et al. 2014, and references therein). Our study supports these results, as the relationship between $f_2$ and $N_H$ that we find implies that the dust and most of the X-ray absorbing gas are at least geometrically related and plausibly belong to the same structure, the putative torus.

4.3. $f_2$ versus AGN Luminosity

Numerous works in the literature find that the relative fraction of type 2 AGNs decreases with increasing AGN luminosity (e.g., Hasinger et al. 2005; Della Ceca et al. 2008; Treister et al. 2008; Ebrero et al. 2009; Burlon et al. 2011; Ueda et al. 2014; Assef et al. 2015; Buchner et al. 2015; Lacy et al. 2015). These results have often been interpreted in the framework of the “receding torus” model. According to this model the radius at which the dust sublimates increases with

\[ L_2 < 10^{46.0} \]

\[ N_H < 4 \times 10^{23} \]

\[ 4 \times 10^{23} \text{ cm}^{-2} < N_H < 10^{24} \text{ cm}^{-2} \]

\[ N_H > 4 \times 10^{23} \]

\[ 10^{23} \text{ cm}^{-2} \leq N_H < 10^{24} \text{ cm}^{-2} \]

\[ 10^{24} \text{ cm}^{-2} \leq N_H < 10^{25} \text{ cm}^{-2} \]

\[ N_H > 10^{25} \text{ cm}^{-2} \]

\[ 10^{25} \text{ cm}^{-2} \leq N_H < 10^{26} \text{ cm}^{-2} \]

\[ N_H > 10^{26} \text{ cm}^{-2} \]

\[ 10^{26} \text{ cm}^{-2} \leq N_H < 10^{27} \text{ cm}^{-2} \]

\[ N_H > 10^{27} \text{ cm}^{-2} \]

\[ 10^{27} \text{ cm}^{-2} \leq N_H < 10^{28} \text{ cm}^{-2} \]

\[ N_H > 10^{28} \text{ cm}^{-2} \]

\[ 10^{28} \text{ cm}^{-2} \leq N_H < 10^{29} \text{ cm}^{-2} \]

\[ N_H > 10^{29} \text{ cm}^{-2} \]

\[ 10^{29} \text{ cm}^{-2} \leq N_H < 10^{30} \text{ cm}^{-2} \]

\[ N_H > 10^{30} \text{ cm}^{-2} \]

\[ 10^{30} \text{ cm}^{-2} \leq N_H < 10^{31} \text{ cm}^{-2} \]

\[ N_H > 10^{31} \text{ cm}^{-2} \]

\[ 10^{31} \text{ cm}^{-2} \leq N_H < 10^{32} \text{ cm}^{-2} \]

\[ N_H > 10^{32} \text{ cm}^{-2} \]

\[ 10^{32} \text{ cm}^{-2} \leq N_H < 10^{33} \text{ cm}^{-2} \]

\[ N_H > 10^{33} \text{ cm}^{-2} \]
AGN luminosity, resulting in an increase of the opening angle of the torus and a decrease of its geometrical covering factor (Lawrence 1991). The end result is that the probability of finding an AGN as an optical type 2 is lower at high AGN luminosities.

To investigate whether we find any evidence supporting a scenario where the AGN radiation field can affect the torus properties, we have determined the distributions of f2 in two luminosity bins. The results are illustrated in Figure 5. We clearly see that low covering factors are preferred in type 1 AGNs at high AGN luminosities. Although a similar trend is detected in type 2 objects, it is much less significant. This is somewhat expected, as a decrease in the torus covering factor reduces the probability of identifying an AGN as optical type 2. We have compared the distributions of f2 obtained at low and high AGN luminosities for the same class of objects using the KS test. We can reject the null hypothesis that the two samples are drawn from the same parent population only for type 1 AGNs with a significance of 99.91%.

Our sample of type 1 AGNs reaches z ∼ 1.7 while all type 2 AGNs have z < 1. To avoid comparing objects at different evolutionary stages, we have also determined the distributions of f2 in our two luminosity bins using type 1 and type 2 objects at z < 1. Our results do not change. We note that we reach the same conclusion, adopting even lower redshift limits. This shows that although the rest-frame infrared spectral regions sampled with our photometric data vary with the objects’ redshift, this has no effect on the f2 distributions presented in Figure 5. Therefore, we can conclude that our results are robust and they are consistent with a decrease of the covering factor of AGN tori with increasing AGN luminosity, although for X-ray-selected type 2 AGNs, the effect is modest. A detailed investigation of whether the detected changes of f2 with luminosity are strong enough to explain the observed scarcity of type 2 AGNs at high luminosities will be presented in a forthcoming paper.

4.4. Nuclear Infrared Continuum Emission

4.4.1. Dependence on f2

It is reasonable to expect that the properties of the nuclear infrared continuum emission of AGNs, in particular the broadband continuum shape, might depend directly on the covering factor of the torus. To investigate this issue we show in Figure 6 (top plots) a compilation of all nuclear infrared SEDs of our AGNs.12 As we are only interested in examining the continuum shape, we have normalized all SEDs at rest-frame 6 μm to facilitate the comparison. To do so we have used linear interpolation in log-log space. We stress that we are only interested in the emission associated with the dusty torus, hence as indicated before, our nuclear infrared SEDs have been corrected for any contamination from the extrapolated accretion disk emission, and of course, the host galaxy.

The first result from Figure 6 is that there is a large range of torus-only infrared continuum shapes for both type 1 and type 2 AGNs. Clearly, at rest-frame wavelengths shorter than ∼20 μm there is no canonical infrared slope for either AGN class (for similar results see also Alonso-Herrero et al. 2003; Lira et al. 2013). More importantly, we find that type 1 and type 2 AGNs show a similar range of infrared continuum slopes, although on average type 2 AGNs have steeper SEDs.

To investigate the role of the torus covering factor we have compared the SEDs of objects with tori with low (f2 < 0.5) and high (f2 > 0.5) covering factors, respectively. To assign the objects to the f2 < 0.5 or f2 > 0.5 class we have used the median values of the posterior distributions of f2 obtained with the BayesCLUMPY SED fits for each source. We then moved all individual SEDs to rest-frame wavelengths and distributed the photometric data points into a common wavelength grid. The bins were defined to have at least 13 points and a minimum size of 0.01 μm. We have used the Astronomy Survival Analysis package (ASURV; Isobe et al. 1986) to determine the median flux values in each bin, taking into account both detections and upper limits. To determine the errors of the median SEDs while fully taking into account both the dispersion and errors in the individual fluxes, we used Monte Carlo simulations. For each photometric point, if it was an upper limit, we kept the values unchanged, while for detections we generated random numbers using Gaussian distributions of mean and sigma, the flux measurements, and their

12 The upper limits indicate cases where, based on our SED decomposition analysis, the AGN accretion disk and host galaxy emission account for the full observed flux. In such cases the upper limit is the combined error of the fluxes associated with the accretion disk and host galaxy emission.
corresponding uncertainties, respectively. In cases where the simulated flux values were lower than zero, we replaced them with the corresponding flux uncertainties and treated them as upper limits. We repeated the Monte Carlo exercise 10⁴ times, each time calculating median fluxes in the bins using the ASURV package, as we did for the real data. We then determined the uncertainties in our median SED fluxes using the 16th and 84th percentiles (68% enclosed, equivalent to 1σ) of the distributions of simulated flux values on each bin. The results of this analysis are illustrated in Figure 6 (bottom plots).

Figure 6. Top plots: nuclear torus-only infrared SEDs of our type 1 (left) and type 2 (right) AGNs, respectively (small open symbols). Downward arrows represent upper limits. All SEDs are normalized at rest-frame 6 μm. Bottom plots: median SEDs of objects with low (f₂ < 0.5; large filled squares) and high (f₂ > 0.5; large filled circles) dust covering factors, respectively. The insets show the fits of the median SEDs of type 1 and type 2 objects with f₂ < 0.5 with a two-component phenomenological model consisting on a power law (PL; dotted line) and a blackbody (BB; dashed line). Solid lines represent the best-fit model (see Section 4.4.2 for details).

Interestingly, we find that ~20% of type 1 AGNs have tori with large, f₂ > 0.5, covering factors, while ~28% of type 2 AGNs have tori with small, f₂ < 0.5, covering factors. As pointed out in Section 2, Seyfert 1.9 objects can only be identified up to z ≤ 0.4 hence, some might still be present in our sample of type 2 AGNs. To evaluate whether this has any impact on our results we have determined the fraction of type 2 AGNs at z < 0.3 that have tori with f₂ < 0.5, finding a value of 22.7% (10 out of 44 objects). We can safely conclude that ~23%–28% of type 2 AGNs have tori with small, f₂ < 0.5, covering factors.

To investigate whether differences exist in the continuum emission of AGN tori as a function of f₂ across the full range of wavelengths sampled, we have determined the spectral index that best describes the broadband continuum emission of AGN tori at rest-frame 5–20 μm. We have used a phenomenological model consisting of a simple power law¹³ that provides a good description of the data at these wavelengths. The results are shown in column 5 in Table 2. Although the numbers are broadly consistent, within the uncertainties, we find that type 2 AGNs have, on average, steeper spectral indices than type 1 AGNs. This is expected because even within the chosen f₂ bins, we characterize the rest-frame 5–20 μm continuum as f_ν ∝ ν⁻α, where α is the power-law index, ν are frequencies, and f_ν are flux densities, respectively.

¹³ We characterize the rest-frame 5–20 μm continuum as f_ν ∝ ν⁻α, where α is the power-law index, ν are frequencies, and f_ν are flux densities, respectively.
the former AGN class has tori with higher covering factors overall than the latter. Clearly, at rest-frame wavelengths longer than 5 μm differences still exist in the continuum emission of AGN tori, even among AGNs of the same optical class.

Although, based on the shape of the torus continuum emission, type 1 and type 2 AGNs are statistically different, there is no sharp division between the nuclear infrared SEDs of the two AGN populations. This implies that from the torus continuum emission alone, we cannot unambiguously distinguish type 1 and type 2 AGNs.

Based on our results we can conclude that the covering factor of the torus is one of the main physical parameters controlling the shape of the nuclear infrared continuum emission of AGNs. Significant differences exist in the properties of the torus emission, even among AGNs of the same optical class, implying that infrared flux-limited population studies at rest-frame wavelengths shorter than ~5–6 μm are not free of biases against the AGN with tori with the highest covering factors. We have shown in Section 4.2 that these objects are, on average, the most highly absorbed AGNs in X-rays.

4.4.2. Near-infrared Hot Dust Emission

A broad near-infrared bump above the extrapolation of the rest-frame >5 μm continuum is clearly detected in the SEDs of our type 1 and type 2 AGNs with tori with low covering factors at rest-frame wavelengths ~1–4 μm. The physical origin of such feature is still not clear. It could be associated with thermal radiation from hot dust in the innermost part of the torus heated by the AGN radiation field and with near sublimation temperatures (for graphite-type and silicate-type grains) or, alternatively, it might be emission from hot dust not associated with the torus (e.g., in the Narrow Line Region; Edelson & Malkan 1986; Barvainis 1987; Minezaki et al. 2004; Kishimoto et al. 2007; Schweitzer et al. 2008; Mor et al. 2009; Riffel et al. 2009; Mor & Netzer 2012).

We have fitted the rest-frame 1–20 μm median SEDs of our type 1 and type 2 AGNs with low torus covering factors with a two-component phenomenological model consisting of a power law and a blackbody to account for the near-infrared bump. We stress that this model is not physically motivated, nor are we claiming that the near-infrared bump originates in a separate component from the torus. Indeed, we find acceptable fits for all torus-only SEDs at rest-frame 1–20 μm with the N08 models, and after a careful visual check of the results from BayesCLUMPY, we find no evidence for additional components. The goal of our exercise is to compare the properties of the nuclear hot dust emission in type 1 and type 2 AGNs. The results of the fits are illustrated in Figure 6 (insets in the bottom plots).

The results obtained for the mean spectral indices of the mid-infrared broadband continuum and blackbody temperatures are $\alpha = 1.87 \pm 0.07$ and $T = 1154.2 \pm 33.2$ K for type 1 AGNs and $\alpha = 1.95 \pm 0.12$ and $T = 1180.1 \pm 81.0$ K for type 2 AGNs. The best-fit temperatures indicate emission from very hot dust close to sublimation temperature. To determine the strength of the near-infrared bump we have computed its relative contribution to the integrated flux at rest-frame 2–7 μm. We found a contribution of 49.5 ± 3.4% in type 1 AGNs and 41.6 ± 6.5% in type 2 AGNs, respectively. Clearly, not only is the near-infrared bump not exclusively detected in type 1 AGNs, but it also appears to have the same overall shape in type 1 and type 2 AGNs with tori with low covering factors.

4.4.3. Contamination from the Accretion Disk and AGN Hosts

So far we have analyzed nuclear infrared SEDs corrected for contamination from the extrapolated accretion disk emission and the AGN host galaxies. To compare our results with previous studies in the literature, which normally do not apply these corrections, we have analyzed the median AGN SEDs that also include the emission from the accretion disk, and the median AGN SEDs based on the cataloged photometry that include also the host galaxy emission. To do so we have followed the same approach as in Section 4.4.1, fitting the rest-frame 5–20 μm continuum emission with a simple power law. The results are summarized in columns 6 and 7 in Table 2. Only when we used median SEDs based on cataloged fluxes did we obtain spectral indices consistent with the typical values reported in the literature, especially for type 1 AGNs (e.g., Alonso-Herrero et al. 2006; Buchanan et al. 2006; Hernán-Caballero et al. 2009; Wu et al. 2009; Mullaney et al. 2011). This demonstrates that not only the emission from the accretion disk but also the stellar emission from the hosts can have a significant impact on the measured best-fit spectral indices of the infrared emission of AGN tori.

5. DISCUSSION AND CONCLUSIONS

Our study aims to test AGN unified models in the framework of clumpy torus models. To do so we have determined the distribution of dust covering factors of AGN tori using a large, uniformly selected, complete sample of 227 AGNs. The AGNs belong to the Bright Ultra-hard XMM-Newton Survey and have

| Class | $f_0$ | $N$ | ($L_\alpha$) | $\alpha$ | $\alpha_{\text{torus}}$ | $\alpha_{\text{torus+disk}}$ | $\alpha_{\text{obs}}$ |
|-------|-------|-----|-------------|---------|----------------|---------------------|----------------|
| Type 1 | All | 132 | 44.34 | 1.48 ± 0.06 | 1.34 ± 0.07 | 1.22 ± 0.07 |
| Type 1 | <0.5 | 106 | 44.41 | 1.40 ± 0.08 | 1.27 ± 0.08 | 1.14 ± 0.08 |
| Type 1 | >0.5 | 26 | 43.74 | 1.99 ± 0.13 | 1.70 ± 0.14 | 1.58 ± 0.11 |
| Type 2 | All | 78 | 43.49 | 1.80 ± 0.07 | 1.74 ± 0.07 | 1.47 ± 0.08 |
| Type 2 | <0.5 | 22 | 43.95 | 1.61 ± 0.13 | 1.55 ± 0.14 | 1.23 ± 0.14 |
| Type 2 | >0.5 | 56 | 43.46 | 1.86 ± 0.08 | 1.81 ± 0.09 | 1.52 ± 0.10 |

Note. (1): optical spectroscopic classification; (2): interval of torus geometrical covering factors of the sample; (3): number of objects; (4): median X-ray luminosity in logarithmic units; (5), (6), and (7): power-law indices of the median infrared continuum at rest-frame 5–20 μm in the following cases: the SEDs include only the emission associated with the torus (column 5); the SEDs include the emission associated with both the torus and the accretion disk (column 6); the SEDs include the emission associated with both the torus and the accretion disk and have not been corrected for any contamination associated with the host galaxies (column 7).
z in the range 0.05–1.7, and 2–10 keV intrinsic (absorption-corrected) luminosities between 10^{32} and 10^{46} erg s^{-1}.

Applying data from UKIDSS, 2MASS, and WISE and a thorough SED decomposition analysis to AGN and galaxy emission, in a previous paper we determined the rest-frame 1–20 μm continuum emission associated with the torus for our sample objects. Here we modeled our nuclear infrared SEDs emission, using the code BayesCLUMPY. This program has been particularly developed to analyze the emission of AGN tori with the Nenkova et al. (2008a, 2008b) models using a Bayesian inference approach.

The main results of our analysis can be summarized as follows.

1. Type 1, type 2, and probably also intermediate-type AGNs, are on average intrinsically different. Type 2 AGNs have tori with higher geometrical covering factors \( f_2 \) on average than type 1 AGNs. Nevertheless, the distributions of \( f_2 \) for both type 1 and type 2 AGNs are broad and there is a large overlap between the two populations. Although rare among all AGNs, we find type 1 objects with large torus covering factors (26 out of 132) and type 2 objects with small torus covering factors (22 out of 78).

2. Interestingly, type 1 and type 2 AGNs with similar levels of X-ray absorption have significantly different distributions of torus geometrical covering factors. This result also holds for X-ray unabsorbed type 1 and type 2 objects.

3. AGNs classified as Sy1.8–1.9 have a rather flat distribution of \( f_2 \) that is significantly different from those of type 1 and type 2 AGNs. Taking into account the fact that most Sy1.8–1.9s are absorbed in X-rays (12 out of 17 objects) it is unlikely that all Sy1.8–1.9 are simply ordinary type 1 AGNs caught in a low flux state during the UV/optical spectroscopic observations. Our results favor a scenario where most Sy1.8–1.9s have broad-line regions reddened by optically thin dust located either in the torus or on physical scales of the narrow-line region or the host galaxies.

4. \( f_2 \) increases with the X-ray column density, at least at \( N_{\text{H}} > 10^{21} \text{cm}^{-2} \), which implies that dust extinction and X-ray absorption are geometrically related and plausibly belong to the same structure, the putative dusty torus.

5. Low \( f_2 \) values are preferred at high AGN luminosities, as postulated by simple receding torus models, although for X-ray-selected type 2 AGNs, the effect is certainly small.

6. Based on our results, \( f_2 \) is one of the main physical parameters controlling the shape of the nuclear infrared emission of AGNs. Although, from the shape of the torus continuum emission, type 1 and type 2 AGNs are statistically different, there is no sharp division between the nuclear infrared SEDs of the two AGN populations. This implies that from the torus continuum emission alone, we cannot unambiguously distinguish type 1 and type 2 AGNs.

7. A broad near-infrared bump at rest-frame \( \sim 1–4 \mu m \) above the extrapolation of the rest-frame \( >5 \mu m \) infrared continuum is clearly detected in the SEDs of our type 1 and type 2 AGNs having tori with low covering factors. We find that such a spectral feature, which is often assumed to be due to hot dust in the innermost part of the torus, is not exclusively detected in type 1 AGNs and it has the same average properties in type 1 and type 2 AGNs.

Based on the results presented here, all AGNs are not intrinsically the same. This result applies not only to AGNs with different optical classifications, but also to objects of the same optical class, in agreement with predictions from clumpy torus models. The AGN radiation field can modify the covering factor of the nuclear dust obscuring the central engine, although, at least in X-ray-selected type 2 objects, the effect is rather small. Furthermore, for AGNs with X-ray absorption in the Compton-thin regime, the covering factor of the torus increases with the X-ray column density.

The reported significant differences in the torus emission, even among AGNs of the same optical class, imply that infrared flux-limited population studies at rest-frame wavelengths shorter than \( \sim 5–6 \mu m \) are not free of biases against the most highly absorbed AGNs, which we have shown are the objects with tori with the highest covering factors.

We can conclude that, the viewing angle, AGN luminosity and also \( f_2 \) determine the optical appearance of an AGN. Furthermore, \( f_2 \) controls the overall shape of the nuclear infrared continuum emission at rest-frame \( \sim 1–20 \mu m \). Thus, the geometrical covering factor of the dusty torus must be incorporated as a key ingredient of unification schemes.

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