AN OFF-CENTER DENSITY PEAK IN THE MILKY WAY’S DARK MATTER HALO?

MICHAEL KUHLEN1, JAVIERA GUEDES2, ANNALISA PILLEPICH3, PIERO MADALI2, AND LUCIO MAYER4

1 Theoretical Astrophysics Center, University of California Berkeley, Hearst Field Annex, Berkeley, CA 94720, USA; mk@astro.berkeley.edu
2 ETH Zurich, Institute for Astronomy, Wolfgang-Pauli-Strasse 27, Zurich 8049, Switzerland
3 Department of Astronomy & Astrophysics, University of California Santa Cruz, 1156 High St., Santa Cruz, CA 95064, USA
4 University of Zurich, Institute for Theoretical Physics, Zurich 8057, Switzerland

Received 2012 August 23; accepted 2012 December 26; published 2013 February 11

ABSTRACT

We show that the position of the central dark matter (DM) density peak may be expected to differ from the dynamical center of the Galaxy by several hundred parsecs. In Eris, a high-resolution cosmological hydrodynamics simulation of a realistic Milky-Way-analog disk galaxy, this offset is 300–400 pc (~3 gravitational softening lengths) after \( z = 1 \). In its dissipationless DM-only twin simulation ErisDark, as well as in the Via Lactea II and GHalo simulations, the offset remains below one softening length for most of its evolution. The growth of the DM offset coincides with a flattening of the central DM density profile in Eris inward of ~1 kpc, and the direction from the dynamical center to the point of maximum DM density is correlated with the orientation of the stellar bar, suggesting a bar–halo interaction as a possible explanation. A DM density offset of several hundred parsecs greatly affects expectations of the DM annihilation signals from the Galactic center. It may also support a DM annihilation interpretation of recent reports by Weniger and Su & Finkbeiner of highly significant 130 GeV gamma-ray line emission from a region 1.5 (~200 pc projected) away from Sgr A* in the Galactic plane.

Key words: dark matter – Galaxy: center – Galaxy: halo – gamma rays: galaxies – methods: numerical

Online-only material: color figures

1. INTRODUCTION

Dissipationless (dark matter only) \( N \)-body simulations predict a nearly universal density profile of dark matter (DM) halos, the so-called NFW profile (Navarro et al. 1997), which features a central \( 1/r \) density cusp. If the cooling and condensation of gas inside these halos (White & Rees 1978; Fall & Efstathiou 1980) is gradual, then so-called adiabatic contraction (Blumenthal et al. 1986; Gnedin et al. 2004) will pull DM into the central regions, thereby increasing the central DM density and further steepening the slope of its density profile. It is thus natural to expect the maximum of the DM density to occur at the dynamical center of a galaxy, the lowest point of its gravitational potential. This expectation has made the Galactic center (GC) a preferred target for indirect DM detection efforts searching for an annihilation signal (Bergström et al. 1998; Gondolo & Silk 1999; Aharonian et al. 2006; Baltz et al. 2008; Danninger & the IceCube collaboration 2012).

As data from the Fermi Gamma-Ray Space Telescope (Atwood et al. 2009) have been accumulating, the number of studies reporting gamma-ray “excesses” or “anomalies” from the GC, which could be interpreted as a DM annihilation signal, has steadily grown (e.g., Goodenough & Hooper 2009; Hooper & Goodenough 2011; Hooper & Linden 2011; Abazajian & Kaplinghat 2012). These analyses have searched for the broad gamma-ray continuum signal thought to arise from the decay and hadronization of DM annihilation products (Bergström et al. 1998). While this is expected to be the dominant DM annihilation signature, it is unfortunately difficult to distinguish it from conventional sources (e.g., millisecond pulsars, Abazajian 2011, or cosmic-ray interactions with molecular clouds, Yusef-Zadeh et al. 2013), and at present a purely astrophysical explanation of these signals cannot be excluded.

More recently, however, there have been surprising reports of a highly statistically significant line-like feature at ~130 GeV in Fermi data from the GC (Bringmann et al. 2012; Weniger 2012; Su & Finkbeiner 2012). Although such a DM annihilation line should be loop-suppressed by a factor \( \sim 10^{-2} \) compared to the expected continuum gamma-ray production in typical DM models, the fact that it is difficult to produce such a high energy line with astrophysical processes (however, see Aharonian et al. 2012) has motivated further exploration of the DM annihilation explanation. In fact, DM particle physics models do exist in which the continuum is suppressed with respect to the line emission (e.g., Cline 2012; Buckley & Hooper 2012; Bergström 2012; Dudas et al. 2012; Chalons et al. 2012). In the analysis of Su & Finkbeiner (2012), the line’s significance is maximized at Galactic coordinates \((\ell, b) = (1.5, 0^\circ)\), i.e., displaced from Sgr A*, the presumed dynamical center of the Galaxy, by about 200 projected pc in the disk plane (see also Tempel et al. 2012). This offset has been viewed as a strike against a DM annihilation interpretation of the line signal. It is possible that the offset is simply due to the small number of statistics (Yang et al. 2012); but nevertheless, it is commonly viewed as a strike against a DM annihilation interpretation of the line signal.

On the other hand, the GC is a dynamically and energetically complex region (Genzel et al. 2010). It harbors a supermassive black hole (SMBH; Ghez et al. 2008; Gillessen et al. 2009), which may have been active as recently as 10 Myr ago, if the giant Fermi bubbles (Dobler et al. 2010; Su et al. 2010) are interpreted as resulting from a black hole accretion event. It is rich in massive young stars (Bartko et al. 2005), and at present a purely astrophysical explanation of these signals cannot be excluded.
In isolated galaxy simulations, resonant interactions between the stellar bar and the DM halo have been shown to alter the shape of DM halos reducing their triaxiality (Berentzen et al. 2006; Machado & Athanassoula 2010), and to flatten a central cusp into a core (Weinberg & Katz 2002; Athanassoula 2003; Holley-Bockelmann et al. 2005; Weinberg & Katz 2007). The latter results remain controversial, however, since other numerical studies do not see such strong effects (Sellwood 2003; Valenzuela & Klypin 2003; Colín et al. 2006). Regarding an off-center DM density peak, these interactions are interesting because they may also induce a “dark bar” and other non-axisymmetric perturbations in the DM (Athanassoula 2002; Ceverino & Klypin 2007; McMillan & Dehnen 2005).

External gravitational perturbations, for example, during a merger or a near passage of a satellite galaxy, could displace the tightly bound baryonic component from the center of the overall mass distribution (the DM halo). Such offsets have been measured in galaxy clusters (Allen 1998), in which separations between the center of the X-ray emitting gas and the gravitational center determined from strong lensing can be as large as ∼30 kpc for relaxed clusters (Shan et al. 2010). A study of THINGS galaxies by Trachternach et al. (2008) found that offsets between the photometric and dynamical centers were less than one radio beam width (∼10″ or 150–700 pc) for 13 out of 15 galaxies with well-constrained photometric centers. However, two galaxies in their sample, NGC 3627 (a barred Sb galaxy) and NGC 6946 (a barred Scd galaxy), exhibit moderate offsets between one and two beam widths.

An offset DM density peak may be a reflection of an intrinsic lopsidedness in the Galaxy (Saha et al. 2009). In fact, disk galaxies commonly exhibit substantial asymmetry in the central regions of their light distribution (for a review, see Jog & Combes 2009). The origin of these asymmetries is not fully understood, with tidal encounters, gas accretion, and a global gravitational instability being some of the physical mechanisms under consideration. The central regions of advanced galaxy mergers often show long-lived unsettled sloshing behavior (Schweizer 1996; Jog & Maybade 2006), and even in isolated galaxies the dynamical center can remain unrelaxed for many dynamical times (Miller & Smith 1992), especially in systems with a cored mass distribution.

Supernova- or active-galactic-nucleus-driven gas outflows may rapidly and non-adiabatically alter the potential in the central regions of proto-galaxies, prior to the formation of the bulk of their stars. Repeated episodes of such impulsive outflows, followed by slow adiabatic re-accretion of gas, may irreversibly transfer energy to the DM, flattening the central cusp in the process (Read & Gilmore 2005; Pontzen & Governato 2012). Although this effect may not by itself produce an off-center DM density peak, the resulting cored density profile will be more susceptible to perturbations.

Lastly, the presence of an SMBH has been argued to lead to the formation of a steep cusp of DM (Gondolo & Silk 1999; Gnedin & Primack 2004) in the inner parsec centered on the SMBH. This would obviously preclude any significant offset between the peak in DM annihilation signal and Sgr A*. In this work we report on the search for the presence of an offset between the dynamical center and the maximum DM density in the Eris simulation (Guedes et al. 2011), one of the highest resolution and most realistic cosmological simulations of the formation of a Milky-Way-like barred spiral galaxy. We find evidence for such an offset, at a scale of 300–400 pc, consistent with the offset seen by Su & Finkbeiner (2012). Since such an offset is only seen in the dissipational hydrodynamic simulations, and not in our collisionless pure-DM runs, we suggest that baryonic physics is in some way responsible for its formation. We examine a number of different physical mechanisms, but the limited resolution of this study does not allow us to conclusively settle on a single preferred explanation.

At this stage, we wish to draw attention to the possibility of the maximum DM density (and hence annihilation luminosity) not being coincident with the dynamical center of our Galaxy, commonly associated with Sgr A*. We hope that our results will stimulate future work, examining other high-resolution hydrodynamic galaxy formation simulations, and investigating in more detail the physical mechanisms that can give rise to an offset DM density peak.

The remainder of this paper is organized as follows. In Section 2 we describe the numerical simulations that we have analyzed. In Section 3 we present the evidence for a DM offset in the Eris simulation. In Section 4 we go over several possible formation mechanisms and confront each of them with data from the simulations. In Section 5 we discuss implications for indirect detection searches toward the GC, and finally in Section 6 we present our conclusions.

2. SIMULATIONS

Our analysis makes use of four cosmological zoom-in simulations of the formation and evolution of a Milky-Way-analog galaxy: one DM-only hydrodynamics simulation, “Eris” (Guedes et al. 2011); and three pure-DM dissipationless simulations, “ErisDark” (A. Pillepich et al. 2013, in preparation), “Via Lactea II” (Diemand et al. 2008), and “GHalo” (Stadel et al. 2009). Details of these simulations are presented in the listed references, and we only briefly summarize their salient features here. Eris and its DM-only twin ErisDark were run with the N-body+SPH code Gasoline (Wadsley et al. 2004), but only Eris utilized the smoothed particle hydrodynamics (SPH). Eris resolves the formation and evolution of a galaxy with 1.3 × 10^8 high-resolution DM particles of mass 9.8 × 10^6 M_⊙ and a similar number of SPH gas particles with an initial mass of 1.2 × 10^4 M_⊙. Gravitational interactions are softened using a cubic spline density kernel of length ϵ_{soft} = 124 proper pc. Throughout the course of the simulation, star particles are created from dense gas (>0.5 atoms cm^{-2}) according to a heuristic star formation recipe with a 10% star formation efficiency. These star particles affect surrounding gas through a supernova (SN) blastwave feedback prescription that injects thermal energy, mass, and metals. The simulation results in a realistic looking barred late-type spiral galaxy, that matches many observational constraints on the structure of the Milky Way. For example, it has a low bulge-to-disk ratio of 0.35, falls on the Tully–Fisher relation, has a stellar-to-total mass ratio of 0.04, and a star formation rate of 1.1 M_⊙ yr^{-1}. Eris is the most realistic such simulation available today.

ErisDark is a DM-only twin to Eris, meaning that it was initialized with the same phases of the Gaussian random density...
These density profiles are centered on the potential minimum. Centering on the point of maximum DM density slightly changes the central slope.
The Astrophysical Journal, 765:10 (13pp), 2013 March 1

Kuhlen et al.

Figure 2. Slices of the central 2 kpc \( \times \) 2 kpc DM density field at \( z = 0 \) through the location of maximum DM density. From left to right: \( x-y, x-z, \) and \( y-z \) planes; from top to bottom: Eris, ErisDark, VL2, and GHalo simulations. The position of the slice in the perpendicular direction is given in the top left corner of every panel. The density field has been smoothed with a Gaussian kernel of width \( \sigma \) equal to one gravitational softening length \( \epsilon_{\text{soft}} = 124, 124, 40, \) and 60 pc, respectively. The \( z \)-axis coincides with the disk normal in Eris, and with the major axis of the prolate DM density ellipsoid in the other cases. The slice thickness is 10 pc for Eris and ErisDark and 5 pc for VL2 and GHalo. The images are centered on the minimum of the total potential (marked with a white cross), while the location of the maximum density is indicated with a red “x.” In the three dissipationless simulations (ErisDark, VL2, and GHalo) the offset between the maximum DM density and the total potential minimum is less than \( \epsilon_{\text{soft}}, \) but it is 2.3 \( \epsilon_{\text{soft}} \) in Eris. (A color version of this figure is available in the online journal.)

Figure 3. The values of \( D_{\text{off}} \) for \( \sigma \ll \epsilon_{\text{soft}} \) are not meaningful, since shot noise can lead to unphysical density spikes on very small scales. But for \( \sigma \gtrsim \epsilon_{\text{soft}} \) the conclusions are robust: the DM offset remains below one \( \epsilon_{\text{soft}}, \) i.e., is consistent with no offset, for all three DM-only simulations regardless of smoothing, while for Eris the offset is greater than \( \epsilon_{\text{soft}} \) up to \( \sigma \approx 260 \) pc. That \( D_{\text{off}} \) drops to zero for even higher \( \sigma \) is not surprising, since any density distribution will appear centered when smoothed on sufficiently large scales.

In the bottom panel of Figure 3 we show the maximum value of the density, \( \rho_{\text{max}} \), for our four simulations. Of course \( \rho_{\text{max}} \) is much more sensitive to \( \sigma \) than \( D_{\text{off}} \), since larger smoothing includes contributions from surrounding lower density material. At \( \sigma = \epsilon_{\text{soft}} \), the density peaks at a value of 0.84 \( M_{\odot} \) pc\(^{-3} \) in Eris, about 25% higher than the value (0.67 \( M_{\odot} \) pc\(^{-3} \)) at its dynamical center. In ErisDark \( \rho_{\text{max}} = 0.40 \) \( M_{\odot} \) pc\(^{-3} \), less than half of the peak density in Eris. We caution that the resolution of our numerical simulations is not sufficient to resolve the internal density structure of the offset peak. With a higher resolution run, the peak-to-center density contrast may well be higher.

3.3. Evolution of the DM Offset

We have performed the same analysis described in the previous section on all 400 outputs of the Eris and ErisDark simulations. Figure 4 shows that the offset measured in Eris at \( z = 0 \)
is no fluke, but persists over cosmological timescales. At very early times ($z \gtrsim 2$) there is no offset in either Eris or ErisDark. Starting at $z \approx 1.5$, however, the DM density maximum in Eris starts to depart from the dynamical center. Over a period of about 2 Gyr the DM offset grows to $D_{\text{off}} \approx 340$ pc (about 3 $\epsilon_{\text{soft}}$), where it remains for the remainder of the simulation. In contrast, in the ErisDark simulation $D_{\text{off}}$ remains below 1 $\epsilon_{\text{soft}}$ for almost its entire evolution, albeit with occasional spikes up to $\sim 200$ pc. These results are qualitatively quite similar to those reported by Macciò et al. (2012, 2015) and others.

Figure 3. Dependence of $D_{\text{off}}$ and $\rho_{\text{max}}$ on the width $\sigma$ of the Gaussian density smoothing kernel. The gravitational softening scale $\epsilon_{\text{soft}} = 124$ pc for Eris and ErisDark is indicated with the dotted line. In the dissipationless simulations (ErisDark, VL2, and GHalo) the DM offset remains well below $\epsilon_{\text{soft}}$ for all $\sigma$. In Eris the offset is larger than $\epsilon_{\text{soft}}$ out to $\sigma = 260$ pc (about 2 $\epsilon_{\text{soft}}$). The maximum density is about a factor of two higher in Eris than in ErisDark, and depends only mildly on $\sigma$ for $\sigma > \epsilon_{\text{soft}}$. $\rho_{\text{max}}$ is larger in VL2 due to its higher halo mass.

(A color version of this figure is available in the online journal.)

3.4. Correlation with DM Density Profile Flattening

The growth of the DM density offset appears to be well correlated with a flattening of the central DM density profile in Eris, as demonstrated in Figure 5. The top panels show mean enclosed density profiles in the inner region ($r < 5$ proper kpc) at several output times from $z = 3$ to $z = 0$. We see two notable differences between Eris (left panel) and ErisDark (right). First, the DM densities (plotted in proper units) tend to be higher in Eris than in ErisDark, which is indicative of “adiabatic contraction.” Second, while the enclosed density in ErisDark continues to increase toward smaller radii, the profiles flatten out in Eris, indicating the formation of a core. Note that we use the term “core” loosely, indicating a substantial flattening of the density profile, but not necessarily implying a constant density.

Inner density profiles are notoriously difficult to properly resolve in $N$-body simulations, requiring high force resolution, large particle counts, and accurate time integration with sufficiently small time steps (Power et al. 2003; Zemp et al. 2007; Diemand et al. 2008; Dubinski et al. 2009). In A. Pillepich et al. (in preparation) we investigate the influence of baryons on the full shape of the density profiles in more detail, including convergence studies. We find a convergence radius for the $z = 0$ density profile in ErisDark of 0.9 kpc, corresponding to $r_{5000}$ enclosed particles. The square symbols in the top panel of Figure 5 indicate $r_{5000}$ (the radius enclosing 5000 DM particles) for the different outputs. Note that $r_{5000}$ is significantly farther out than $3 \epsilon_{\text{soft}}$ (indicated with the vertical bars), a commonly used “rule of thumb” for how far in density profiles can be trusted. For Eris, $r_{5000}$ is probably overly conservative, since the potential is dominated by baryons and many more than 5000 gas and star particles are found inside of $r_{5000}$. As an intermediate case, we also mark with circles $r_{1000}$, the radius enclosing 1000 DM particles.

---

$^7$ At $z = 0$, there are over a million star particles within $r_{5000}$ and more than 400,000 within $r_{1000}$. 

---

Figure 4. Time dependence of the DM offset from the total potential minimum in Eris (blue) and ErisDark (red). The gravitational softening $\epsilon_{\text{soft}}(z) = 124$ pc is indicated with a dashed line. In ErisDark the DM offset remains around or below $1 \epsilon_{\text{soft}}$ for almost the entire simulation, while in Eris it begins to significantly exceed $\epsilon_{\text{soft}}$ around $z = 1.5$ and remains at $\approx 3 \epsilon_{\text{soft}}$ afterward.

(A color version of this figure is available in the online journal.)
In the bottom panel of Figure 5 we show the evolution of the logarithmic slope $\frac{d\ln \rho}{d\ln r}$ at radii. We obtained these slopes by first fitting the enclosed density profiles inward of 5 kpc to a modified Burkert profile, 
\begin{equation}
\langle \rho \rangle (r) = \frac{\rho_0 r_c^\alpha}{r^a (r^2 + r_c^2)^{(\beta - a)/2}},
\end{equation}
and then evaluating its logarithmic slope at the radii of interest, 
\begin{equation}
\frac{d\ln \langle \rho \rangle}{d\ln r} = -\alpha + \frac{\alpha - \beta}{1 + (r_c/r)^2}.
\end{equation}
This functional form describes the central enclosed density profile in Eris and ErisDark much better than a constant power law or Einasto profile. Note, however, that this fitting function is designed to track the enclosed density profile all the way down to $\epsilon_{\text{soft}}$, so way beyond the convergence radius. We wish to emphasize that we merely use this fit to evaluate the logarithmic slope at radii outside of $3 \epsilon_{\text{soft}}$, and do not attach any physical meaning to the asymptotic inner slopes $\alpha$ preferred by the fits.

Figure 5 clearly shows that Eris develops a cored density profile, in the sense that it has a much shallower logarithmic slope at $r_{5000}$ than ErisDark. Measured at $r_{5000}$, the log slope in Eris becomes progressively shallower until it stabilizes at a value of $\sim -0.3$ at $z \approx 1$. Note that $r_{5000}$ is larger than $D_{\text{eff}}(z)$ at all redshifts. Measured at $r_{1000}$ the profile even flattens out completely with a log slope of $\sim -0.5$. In ErisDark, on the other hand, the slope at $r_{5000}$ remains close to the NFW value of $-1$ after $z = 1.5$. Comparison with Figure 4 shows that the onset and timescale of the core formation in Eris is remarkably well correlated with the growth of the DM density offset. This is a strong hint that whatever baryonic process drives the core formation may also be responsible for the offset DM density peak.

4. NATURE AND ORIGIN OF THE OFFSET PEAK

The existence of a well-defined offset to the peak of the DM distribution in Eris is unexpected, and its physical nature not immediately apparent. Some possibilities that we have considered are: (1) statistical fluctuations, (2) an incompletely dissolved subhalo core, and (3) excitation of a DM density wave by the stellar bar or other perturber. In the following sections we address these possibilities in turn.

As we have seen, the output cadence of the original Eris simulation is not sufficient to follow the dynamics of the peak. To help with understanding the physical nature of the offset, much higher cadence outputs are desirable. To this end we have restarted the Eris simulation from output number 393 ($z = 0.0151$) with a $\sim 20$ times finer temporal resolution ($\Delta t = 1.43$ Myr) and evolved the simulation for 140 time steps (206 Myr). Visualizations of nine consecutive high cadence outputs, spanning 11.5 Myr, are shown in Figure 6, and a movie of the full evolution can be viewed at http://vimeo.com/45114776.

Visual inspection of these much higher cadence outputs shows that the offset peak appears to sometimes jump around somewhat discontinuously between two subsequent outputs. Occasionally there are multiple peaks of roughly equal density. As already seen with the coarser time resolution, the point of maximum density appears to avoid the very center and remains close to the disk plane.

4.1. Statistical Fluctuations?

As shown in Section 3.3, the growth of the DM offset coincides in time with the formation of a core in the Eris DM distribution. In a constant density core, sampled with a small number of $N$-body particles, Poisson fluctuations can give rise to a spurious density peak offset from the center. The mean DM density in the Eris’ core (inward of 1 kpc) is $0.51 M_\odot \text{pc}^{-3}$, corresponding to an $N$-body particle density of $5300$ particles $\text{pc}^{-3}$. At $z = 0$ there are $509$ particles within $2 \epsilon_{\text{soft}}$ of the location of maximum density, much higher than the expected $306$ for the average core density and well beyond what Poissonian fluctuations can produce. We have numerically confirmed this by constructing $500$ randomly drawn particle distributions with the same mean particle density as the Eris core, and analyzed these samples in the same manner as described above.
Figure 6. 3D contour plots of the DM density in the central (2 kpc)$^3$ volume of Eris. The outer contour (light blue) corresponds to $\rho = 0.45 M_\odot$ pc$^{-3}$, the middle contour (light orange) to $0.8 M_\odot$ pc$^{-3}$, and the opaque innermost contour (red) to the 99th percentile of the DM density in the volume. The dynamical center is marked with a black dot, and the stellar disk lies in the X–Y plane. The images show the time evolution over 11.5 Myr ($\Delta t = 1.43$ Myr) starting from $z = 0.0151$. In the last two frames we have plotted the positions of all 78 particles located within $1 \epsilon_{\text{soft}}$ of the maximum density at the second-to-last output shown. Only 1.43 Myr later (last frame) they have already dispersed throughout the plotted volume, indicating that the density offset is not a bound structure.

(A color version of this figure is available in the online journal.)

In Figure 7 we compare the distributions of $\rho_{\text{max}}$ and $D_{\text{off}}$ between the random samples and the last $\sim 124$ Eris outputs spanning 4 Gyr of evolution. Eris’ $\rho_{\text{max}}$ distribution is peaked at 0.85 $M_\odot$ pc$^{-3}$, way beyond the random distribution, which peaks at 0.61 $M_\odot$ pc$^{-3}$ and has an rms dispersion of only 0.01 $M_\odot$ pc$^{-3}$. Similarly, the $D_{\text{off}}$ probability distribution function for Eris is peaked around 350 pc and looks nothing like that of the random samples, which slowly increases toward larger $D_{\text{off}}$, in accordance with a simple volumetric $D_{\text{off}}^{1/3}$ scaling. These comparisons very clearly demonstrate that the DM offsets we have found in Eris are not due to statistical fluctuations.

4.2. Incompletely Disrupted Subhalo Core?

In this potential explanation, the offset density peak would be identified with the tightly bound central regions of an incompletely disrupted subhalo. The subhalo would have to have been massive enough to have experienced substantial baryonic condensation and associated contraction of its DM, making it more resilient to complete tidal disruption than its DM-only counterpart in ErisDark. If such a halo fell into the host at $z \gtrsim 1.5$, dynamical friction would quickly drag it in to the center, where tidal interactions would have stripped most of the weakly bound material in its outskirt. The inspiral would have stalled once its mass dropped to the point where dynamical friction becomes unimportant. After that point it would continue to orbit around the dynamical center, its temporal cohesion possibly aided by the stabilizing effect of a harmonic potential (Kleyna et al. 2003; Read et al. 2006).

We can rule out this possibility, based on several observations: (1) as mentioned above, there is no stellar counterpart to the DM offset, and (2) the peak persists for hundreds of dynamical times, which seems too long for an orbiting subhalo core to survive. The final nail in the coffin (3) is the fact that the offset DM peak does not appear to be a bound feature. This is demonstrated in the last two panels of Figure 6, in which we show the positions of all 78 particles located within $1 \epsilon_{\text{soft}}$ of the maximum density peak at $t = 10$ Myr (after $z = 0.015$). A mere 1.4 Myr later, these same particles have dispersed throughout the central volume. This implies that the offset density peak is comprised of different particles at different times.
We have examined the motion of the potential minimum in absolute code coordinates (top panel of Figure 8), and do not see any evidence for a sharp kink or abrupt displacement at the time of the satellite’s passage. Furthermore, it appears that the potential minimum is moving smoothly in code coordinates, and it is the DM offset that moves around the potential minimum, not the other way around (bottom panel of Figure 8).

4.4. Density Wave Excitation by the Stellar Bar?

Another possibility is that the DM offset is the result of a density wave excitation of some kind. In this explanation the peak would be contributed by different particles at different times, just as observed, its spatial evolution would be set by whatever external source is providing the excitation, and it may be long lived, provided a continuous excitation mechanism exists. A natural candidate for such an external source would be the stellar bar in Eris. The potential is completely dominated by the stars in the central region, and so it seems plausible that the DM distribution may be affected by departures from axisymmetry in the stellar component. Indeed, resonant interactions between the DM halo and a stellar bar have been invoked to explain the transformation of an initially cuspy DM density profile into a cored one (Weinberg & Katz 2002, 2007). In related work, McMillan & Dehnen (2005) identified an instability in which a rotating stellar bar pinned to the origin causes the DM cusp to move away from the origin. While they used this effect to argue that the observed flattening of the DM density profile may be artificial, their work provides a proof-of-concept for an off-center DM density peak.

In isolated galaxy simulations it has been possible to identify DM halo particles trapped in different resonances (Athanassoula 2002; Ceverino & Klypin 2007; Dubinski et al. 2009). The Inner Lindblad Resonance may lead to the formation of a “dark bar” (Colín et al. 2006; Ceverino & Klypin 2007), which may be showing up in Eris as a DM offset. The ring-like morphology of particles trapped in the corotation resonance (see, e.g., Figure 11 of Ceverino & Klypin 2007) is reminiscent of the distribution of DM in the plane of Eris (see Figure 2). A detailed investigation of the resonant structure of DM particle orbits in Eris is beyond the scope of this paper, but will be pursued in future work.

Arguments in favor of the bar-driven explanation are that the growth of the offset coincides with the formation of a DM core, that the offset peak preferentially lies close to the stellar disk plane, and that the direction from the dynamical center toward the offset density peak appears to be correlated with the orientation of the stellar bar. This last point is demonstrated in Figure 9, which shows distributions of |cos θ|, the angle between the offset peak and the major axis of the stellar density ellipsoid inward of 1 kpc (i.e., the orientation of the stellar bar).

We have split the distributions up by time epoch: during early times (<4 Gyr), prior to the appearance of a significant DM density offset, the distribution is consistent with uniform in |cos θ|, corresponding to a completely random placement of the density peak. Between 4 and 8 Gyr the DM offset first begins to become significantly larger than ϵ_{soft}, and the |cos θ| probability density function is strongly peaked toward unity. Its mean value of ⟨|cos θ|⟩ = 0.83 corresponds to an angle of 34°. At later times, once the DM offset has become established, the correlation weakens slightly, with ⟨|cos θ|⟩ dropping to 0.77, but it still remains preferentially aligned with the bar.

The top panel of Figure 10 shows the results of a frequency scan from ω/2π = 0.1 to 10^3 Gyr^{-1} of the angular evolution of the direction toward the offset. For every frequency ω, we

![Figure 7](image-url)
performed a least-squares fit to a sinusoid for all coarsely sampled outputs after 8 Gyr. The plot of $R^2 = \sum (\theta_{\text{off}}(t_i) - \pi/2 \cos(\omega(t_i - t_0)))^2$ exhibits a distinct low $R^2$ spike at a frequency of $\omega/2\pi = 15$ Gyr$^{-1}$, corresponding to a period of 69 Myr, as well as at several of its harmonics (30, 45, 60 Gyr$^{-1}$, etc.). These spikes indicate the presence of a periodic signal in the offset angle evolution, which is consistent with the alignment of the offset with the orientation of the stellar bar. In the lower panel of Figure 10 we show the best-fit sinusoid overplotted on the offset angle evolution for the 22 outputs since 13 Gyr.

For completeness, we should also mention two problematic aspects of the stellar bar-driven explanation. One is that the strength of stellar bars typically grows and fades with time (Bournaud & Combes 2002), modulated by gas accretion. Indeed this is the case in Eris as well: the amplitude of the $m = 2$ mode in its stellar disk is strongest at $z > 3$, then declines somewhat only to grow again around $z \approx 2$, after which it gradually decreases in strength toward $z = 0$ (see Figure 4 of Guedes et al. 2012). It is not clear then why the DM offset would saturate at around 300–400 pc in the last 8 Gyr, when the strength of the bar is gradually decreasing. The $\sim$340 pc extent of the DM offset is also surprising, since Eris’ stellar bar is several kiloparsecs in length, and its corotation radius occurs at 2.7 kpc. It is clear that more work is needed to fully elucidate the role of a stellar bar interaction in explaining the DM offset.

4.5. Numerical Resolution

At $D_{\text{off}} \approx 3\epsilon_{\text{soft}}$, the scale of the offset is worrisomely close to the force resolution of the simulation. A detailed study of the internal density structure of the offset peak must certainly await much higher resolution hydrodynamic simulations. Nevertheless, the fact that no offset is observed in ErisDark, which has the same force resolution as Eris, gives us some confidence that the existence of an offset DM density peak is no numerical artifact, and indicates that baryonic physics appears to be responsible in some way.

We would like to be able to check whether the offset remains at the same physical scale ($\sim$340 pc) even in a simulation with
Figure 9. Probability distribution functions of the cosine of the angle between the direction toward the DM offset and the orientation of the stellar bar, defined as the major axis of the stellar density ellipsoid inward of 1 kpc. The three panels show the distributions split by cosmic time: early times, prior to the appearance of the DM offset (top panel), an intermediate time period over which the DM offset grows in magnitude (middle), and late times, during which the DM offset remains more or less constant at $\sim 340$ pc (bottom). The early distribution is consistent with uniform in $|\cos \theta|$, whereas once the DM offset becomes pronounced the distributions prefer large values of $|\cos \theta|$, indicating alignment between the offset peak and the stellar bar.

(A color version of this figure is available in the online journal.)

a smaller gravitational softening length. At the moment we do not have access to such a simulation, but we can go in the opposite direction and look at a lower resolution run. We have run ErisLores and ErisDarkLores at eight times poorer mass resolution ($7.8 \times 10^5 M_\odot$ and $9.5 \times 10^5 M_\odot$, respectively) and with a four times larger gravitational softening length, $\epsilon_{\text{soft}} = 495$ pc. We have analyzed these simulations in the same way as described above, except that all length scales have been increased by a factor of four to account for the larger $\epsilon_{\text{soft}}$.

We CIC-deposit particles onto a grid with a cell width of 40 pc and smooth the density field with a Gaussian kernel with $\sigma = \epsilon_{\text{soft}} = 495$ pc.

As with the higher resolution simulations, we find that the point of maximum density is displaced from the minimum of the potential in ErisLores: $D_{\text{off}} = 430$ pc at $z = 0.15$ and $650$ pc at $z = 0$. And again the DM-only counterpart ErisDarkLores has a much smaller offset, $D_{\text{off}} = 60$ pc. Although $D_{\text{off}}$ is somewhat larger in ErisLores than in Eris in absolute terms, it is clear that the offset is not scaling linearly with $\epsilon_{\text{soft}}$: while $D_{\text{off}} \approx 3\epsilon_{\text{soft}}$ in Eris, it is only $1\sim 1.5 \epsilon_{\text{soft}}$ in ErisLores.

We have also checked time steps and energy conservation in our simulations, as insufficiently short time steps can lead to the formation of a spurious density core (Zemp et al. 2007; Dubinski et al. 2009). The Eris simulation suite uses adaptive time steps that scale as $\sqrt{\epsilon_{\text{soft}}/a}$, where $a$ is the acceleration of a particle, as recommended by Power et al. (2003). This results in time steps as small as 0.16 Myr at low redshift, which is three times smaller than the fixed time step that Dubinski et al. (2009) employed in a simulation with comparable $\epsilon_{\text{soft}}$ (their model m100K), and which they found to be short enough to avoid the formation of an artificial core.

These checks give us further confidence that the DM offset we have observed in Eris cannot be attributed solely to insufficient numerical resolution or time stepping. On the other hand, we cannot claim to have fully resolved $D_{\text{off}}$ either—higher resolution studies are needed.

4.6. The Role of the Central DM Core

It is clear that the central DM core plays an important role for the formation of an off-center DM density peak. Without a flattened central density profile it may be difficult to excite an offset peak, since any non-central density enhancement would be overwhelmed by the steeply rising central cusp. Indeed, as we have seen above, the growth of the DM offset temporally coincides with the formation of such a core. We have not yet determined what physical processes led to the formation of this core in Eris.

A core formation mechanism that has recently been suggested is the repeated removal of large amounts of gas from the central regions through the action of violent SN explosions (Read & Gilmore 2005; Pontzen & Governato 2012). If these baryonic outflows abruptly alter the potential, the DM may respond by...
flowing out of the center, transforming the cusp into a core in the process. Perhaps this DM redistribution could also create a \( R \) core with radius \( r_0 \) kpc, which, if seen edge on, would correspond to an angular offset of 2.4 deg. For comparison, the search for a DM annihilation signal using the H.E.S.S. imaging Atmospheric Cherenkov Telescope was restricted to a region of 45–150 pc in projected distance from the GC (Abramowski et al. 2011). In this context, the recent report of a highly significant detection of a gamma-ray line at 127±2 GeV in Fermi data from the GC (Su & Finkbeiner 2012) is particularly intriguing. Su & Finkbeiner (2012) report that the signal is maximized at a Galactic longitude of \( \ell \approx 1.5 \) deg. While this offset may have initially been viewed as a strike against a DM annihilation interpretation of the line, our work demonstrates as a proof-of-principle that just such an offset should perhaps be expected.

In Figure 11 we show the DM annihilation luminosity \( \int \rho_\text{DM}^2 \ell \), calculated from the central (2 kpc) \(^3\) region in Eris. The view is through the disk plane (the vertical axis corresponds to the disk normal) and the coordinate system has been rotated such that the offset peak is viewed edge-on, i.e., maximizing the angular offset. As before, the 3D density grid was first smoothed with a Gaussian kernel of width \( \sigma = 0.5 \) kpc. We then squared it, multiplied the cells by their volume to get not the only core formation mechanism, highlighting a possible important difference between the evolution of Milky-Way-sized galaxies and that of the dwarf galaxies described by Governato et al. (2010, 2012). Instead, perhaps the stellar bar may be responsible for this transformation, through resonant angular momentum exchange between the bar and the DM as suggested by Weinberg & Katz (2002, 2007). Clearly, a more detailed investigation of the DM core formation process in Eris is needed, and will be the topic of a future study.

5. DISCUSSION

Provided that the central DM distribution in the Eris simulation is representative of that in our Milky Way, the results we have presented here have several important consequences for indirect DM detection efforts aimed at the GC.

The first consequence concerns the shape of the DM density profile used to predict the annihilation luminosity from the central regions of the Galaxy. Outside of \( \sim 1 \) kpc, the DM density profile in both Eris and ErisDark (as well as VL2 and GHalo) is well described by an NFW or Einasto profile. However, cooling and condensation of gas in Eris has dragged DM toward the center, such that the normalization of the density profile in Eris is larger than in ErisDark: at 1 kpc the mean enclosed DM density is 2.7 times higher in Eris (0.52 \( M_\odot \) pc\(^{-3}\)) than in ErisDark (0.20 \( M_\odot \) pc\(^{-3}\)). At angles greater than \( \sim 7 \) deg from the GC, one may thus expect baryonic processes to lead to a significant enhancement of the surface brightness of diffuse radiation arising from DM annihilation.

As discussed in Section 3.4, at even smaller radii baryonic physics leads to the formation of a DM core in Eris, and as a result, the mean enclosed DM density in Eris never rises to more than 0.73 \( M_\odot \) pc\(^{-3}\). For comparison, an extrapolation of the best-fitting Einasto profile for ErisDark reaches 1 \( M_\odot \) pc\(^{-3}\) at 200 pc, 10 \( M_\odot \) pc\(^{-3}\) at 3 pc, and asymptotes to 90 \( M_\odot \) pc\(^{-3}\). We thus caution against extrapolating density profiles determined from dissipationless DM-only simulations (such as Via Lactea II, GHalo, and Aquarius) all the way in to the GC in order to infer central annihilation luminosities.

Second, a maximum in the DM density that is not coincident with the dynamical center of the Galaxy significantly modifies expectations for where the central surface brightness of DM annihilation radiation should peak. The time-averaged value of \( D_{\text{off}} \) in Eris is 340 pc, which, if seen edge on, would correspond to an angular offset of 2.4 deg. For comparison, the search for a DM annihilation signal using the H.E.S.S. imaging Atmospheric Cherenkov Telescope was restricted to a region of 45–150 pc in projected distance from the GC (Abramowski et al. 2011). In this context, the recent report of a highly significant detection of a gamma-ray line at 127±2 GeV in Fermi data from the GC (Su & Finkbeiner 2012) is particularly intriguing. Su & Finkbeiner (2012) report that the signal is maximized at a Galactic longitude of \( \ell \approx 1.5 \) deg. While this offset may have initially been viewed as a strike against a DM annihilation interpretation of the line, our work demonstrates as a proof-of-principle that just such an offset should perhaps be expected.

Figure 10. Top: frequency scan of the angular evolution of the direction toward the DM offset. \( R^2 \) is the sum of the squared differences between the best-fit sinusoid of frequency \( \omega \) and the angular position of the DM offset. Lower values of \( R^2 \) indicate a better fit, and the deep spike to \( R^2 < 1 \) at \( \sim 15 \text{ Gyr}^{-1} \) corresponds to a periodicity of 69 Myr in the angular evolution. Bottom: the best-fitting sinusoid (red) overplotted on angular position of the DM offset in the last 22 outputs.

(A color version of this figure is available in the online journal.)
Figure 11. DM annihilation luminosity “surface density” ($\int \rho_{\text{DM}}^2 \, d\ell$) in the central 2 kpc $\times$ 2 kpc region of Eris. The contrast between the dynamical center (white plus) and the peak (red cross) is $\sim$11%. The vertical axis corresponds to the disk normal, and the coordinate system has been rotated to maximize the angular offset of the peak.

(A color version of this figure is available in the online journal.)

a luminosity, summed them up along the Y-axis, and finally divided the resulting map by the area of each cell to get a surface density$^9$ in units of $M_\odot^2 \text{pc}^{-5}$. This map does not take into account any luminosity produced by DM along the line of sight outside the central cube.

The contrast between the maximum of the map ($870 M_\odot^2 \text{pc}^{-5}$) and the center ($780 M_\odot^2 \text{pc}^{-5}$) is only about 11% at $z = 0$. Furthermore there is a second subdominant peak to the left of the center with a luminosity surface density of $830 M_\odot^2 \text{pc}^{-5}$, only 5% less than the global maximum. If anything, the contrast at $z = 0$ is a bit of an outlier, as the mean contrast between offset peak and GC over the past 4 Gyr is only $\sim$5% with a 3% standard deviation. The greatest contrast measured over all outputs is 15%. Such small contrasts may not be compatible with the measurement of Su & Finkbeiner (2012), but it is important to keep in mind that the internal structure of the peak is certainly not resolved in the simulation. It is conceivable that the contrast would increase with higher resolution, especially if resonances with the stellar bar are responsible, since those would be spread out artificially at low resolution.

6. CONCLUSIONS

We have analyzed the distribution of DM in the central regions of the hydrodynamical galaxy formation simulation Eris, one of the highest resolution and most realistic simulations to date of the formation of a barred spiral galaxy like our own Milky Way. Surprisingly, we find that the peak of the DM density in Eris is typically offset from its dynamical center by several hundred parsecs. No such offset is observed in its DM-only twin simulation ErisDark, nor in the much higher resolution DM-only Via Lactea II and GHalo simulations.

The DM offset in Eris begins to appear around $z = 1.5$ and grows over a period of 2 Gyr to a stable value of $\langle D_{\text{off}} \rangle = 340$ pc (almost three gravitational softening lengths), with a dispersion of 50 pc. The onset and duration of the DM offset appears to be well correlated with the formation of a nearly constant DM density core. The distributions of $\rho_{\text{max}}$ and $D_{\text{off}}$ over the past 4 Gyr are inconsistent with a statistical fluctuation. Neither is the density peak a gravitationally bound structure, which rules out an incompletely disrupted subhalo core as an explanation. The most likely explanation may be a density-wave-like excitation by the stellar bar, possibly related to the resonant mechanism proposed by Weinberg & Katz (2002, 2007) to explain the transformation of a central DM cusp into a core. Arguments in favor of this explanation are the fact that the DM offset appears preferentially near the disk plane, that it is aligned to $\sim$30 deg with the orientation of the stellar bar, and that it shows a periodicity of $\sim$70 Myr.

A central DM offset is of particular interest in the context of the recent report by Su & Finkbeiner (2012) of a highly significant detection of gamma-ray line emission from a region $\sim$1.5 deg ($\sim$200 pc projected) away from the GC. At first impression, such a large angular offset would seem to argue against a DM annihilation interpretation of this signal. Our work demonstrates that, in fact, just such an offset should perhaps be expected. We note, however, that at the current resolution of our numerical simulations, the low contrast (5%–15%) of the annihilation surface brightness between the offset peak and the GC may be too small to accommodate a DM annihilation explanation.

We conclude by acknowledging that properly resolving the effects of baryonic physics on the central DM distribution, in particular those involving resonant bar-halo interactions, requires much higher resolution than we have been able to afford thus far in cosmological hydrodynamics simulations. Further studies

$^9$ To further clarify, the sum of all 200$^2$ “pixels” multiplied by the total area ($4 \times 10^6 \text{pc}^2$) is equal to the total luminosity emitted from the (2 kpc)$^3$ cube.
at higher resolution and exploring different baryonic physics implementation are sorely needed. Of particular importance are clarifying the role of the star formation threshold parameter and SN feedback for the formation of a DM core, as well as the influence of the supermassive black hole at the GC on the DM distribution.

M.K. thanks Doug Finkbeiner for initially suggesting this analysis and several encouraging exchanges afterward, and Andrey Kravtsov, Daniel Ceverino, Anatoly Klypin, Eliot Quataert, and Justin Read for valuable discussion of these results. J.G. was partially funded by the ETH Zurich Postdoctoral Fellowship and the Marie Curie Actions for People COFUND Program. The high time resolution rerun of Eris was performed under project IDs s205 and s352, and in part by the U.S. National Science Foundation, grants OIA-1124453 (PI: P. Madau) and OIA-1124403 (PI: A. Szalay).

REFERENCES

Abazajian, K. N. 2011, JCAP, 03, 010
Abazajian, K. N., & Kaplinghat, M. 2012, PhRvD, 86, 083511
Abramowski, A., Acero, F., Abdo, A. A., et al. 2009, ApJ, 697, 1071
Aharonian, F., & Kuehnl, M. 2012, PhRvD, 86, 083511
Aharonian, F., Khangulyan, D., & Malyshev, D. 2012, A&A, 547, A114
Allen, S. W. 1998, MNRAS, 296, 392
Amatini, S. 2009, MNRAS, 398, 1210
Atwood, W. B., Abdo, A. A., Ackermann, M., et al. 2009, ApJ, 706, 1071
Balzer, E. A., Berenji, B., Bertone, G., et al. 2008, JCAP, 07, 013
Bartko, H., Martins, F., Fritz, T. K., et al. 2009, ApJ, 697, 1741
Bartko, H., Martins, F., Fritz, T. K., et al. 2009, ApJ, 697, 1741
Berentzen, I., Shlosman, I., & Jogee, S. 2006, ApJ, 637, 582
Bringmann, T., Huang, X., Ibarra, A., Vogl, S., & Weniger, C. 2012, JCAP, 07, 054
Buckley, M. R., & Hooper, D. 2012, PhRvD, 86, 035053
Ceverino, D., & Klypin, A. 2007, MNRAS, 379, 1155
Chalons, G., Dolan, M. J., & McCabe, C. 2012, arXiv:1211.5154
Clune, J. M. 2012, PhRvD, 86, 052002
Collin, P., Valenzuela, O., & Klypin, A. 2006, ApJ, 648, 687
Danninger, M., & the IceCube collaboration. 2012, JPhCS, 375, 012038
Diemand, J., Kuhlen, M., Madau, P., et al. 2008, Natur, 454, 735
Dobler, G., Finkbeiner, D. P., Cholis, I., Slatyer, T., & Weinr, N. 2010, ApJ, 717, 825
Dubinski, J., Berentzen, I., & Shlosman, I. 2009, ApJ, 697, 293
Dudas, E., Mambrini, Y., Poikalsky, S., & Romagnoni, A. 2012, JHEP, 10, 123
Fall, S. M., & Efstatiu, G. 1980, MNRAS, 193, 189
Genzel, R., Eisenhauer, F., & Gillessen, S. 2010, RVMP, 82, 3121
Ghez, A. M., Salim, S., Weinberg, N. N., et al. 2008, ApJ, 689, 1044
Gillessen, S., Eisenhauer, F., Trippe, S., et al. 2009, ApJ, 692, 1075
Gnedin, O. Y., Kravtsov, A. V., Klypin, A. A., & Nagai, D. 2004, ApJ, 616, 16
Gnedin, O. Y., & Primack, J. R. 2004, PhRvL, 93, 61302
Gondolo, P., & Silk, J. 1999, PhRvL, 83, 1719
Goodenough, L., & Hooper, D. 2009, arXiv:0910.2998
Governato, F., Brook, C., Mayer, L., et al. 2010, Natur, 463, 203
Governato, F., Zoletov, A., Portzen, A., et al. 2012, MNRAS, 422, 1231
Guedes, J., Callegari, S., Madau, P., & Mayer, L. 2011, ApJ, 742, 76
Guedes, J., Mayer, L., Carollo, M., & Madau, P. 2012, ApJ, submitted (arXiv:1211.1715)
Holley-Bockelmann, K., Weinberg, M., & Katz, N. 2005, MNRAS, 363, 991
Hooper, D., & Goodenough, L. 2011, PhLB, 697, 412
Hooper, D., & Linden, T. 2011, PhRvD, 84, 123005
Jog, C. J., & Combes, F. 2009, PhR, 741, 15
Jog, C. J., & Maybhate, A. 2006, MNRAS, 370, 891
Klypin, A., Zhao, H., & Somerville, R. S. 2002, ApJ, 573, 597
Macciò, A. V., Stinson, G., Brook, C. B., et al. 2012, ApJL, 744, L9
Machado, R. E. G., & Athanassoula, E. 2010, MNRAS, 406, 2386
Martinez-Valpuesta, I., & Gerhard, O. 2011, ApJL, 734, L20
McMillan, P. J., & Dehnen, W. 2005, MNRAS, 363, 1205
Miller, R. H., & Smith, B. F. 1992, ApJ, 391, 508
Muno, M. P., Bagannock, F. K., Bautz, M. W., et al. 2003, ApJ, 589, 225
Muno, M. P., Pfahl, E., Baganoff, F. K., et al. 2005, ApJL, 622, L111
Navarro, J. F., Frenk, C. S., & White, S. D. M. 1997, ApJ, 490, 493
Paumard, T., Genzel, R., Martins, F., et al. 2006, ApJ, 643, 1011
Porten, A., & Governato, F. 2012, MNRAS, 421, 3464
Power, C., Navarro, J. F., Jenkins, A., et al. 2003, MNRAS, 338, 14
Read, J. I., & Gilmore, G. 2005, MNRAS, 356, 107
Read, J. I., Goert, T. Moore, B., et al. 2006, MNRAS, 373, 1451
Saha, K., Levine, E. S., Jog, C. J., & Blitz, L. 2009, ApJ, 697, 2015
Schweizer, F. 1996, AJ, 111, 109
Sellwood, J. A. 2003, ApJ, 587, 638
Shan, H., Qin, B., Fort, B., et al. 2010, MNRAS, 406, 1134
Stadel, J., Potter, D., Moore, B., et al. 2009, MNRAS, 398, L21
Su, M., & Finkbeiner, D. P. 2012, arXiv:1206.1616
Su, M., Slatyer, T. R., & Finkbeiner, D. P. 2010, ApJ, 724, 1044
Temple, E., Hektor, A., & Raidal, M. 2012, ICAP, 9, 32
Trachternach, C., de Blok, W. J. G., Walter, F., Brinks, E., & Kennicutt, R. C. 2008, AJ, 136, 2720
Valenzuela, O., & Klypin, A. 2003, MNRAS, 345, 406
Wadsley, J. W., Stadel, J., & Quinn, T. 2004, NewA, 9, 137
Weinberg, M. D., & Katz, N. 2002, ApJ, 580, 627
Weinberg, M. D., & Katz, N. 2007, MNRAS, 375, 425
Weniger, C. 2012, ICAP, 8, 7
White, S. D. M., & Rees, M. J. 1978, MNRAS, 183, 341
Yang, R. Z., Yuan, Q., Feng, L., Fan, Y. Z., & Chang, J. 2012, PhLB, 715, 285
Yusef-Zadeh, F., Hewitt, J. W., Wardle, M., et al. 2013, ApJ, 762, 33
Zemp, M., Stadel, J., Moore, B., & Carollo, C. M. 2007, MNRAS, 376, 273