Modeling the Initial Conditions of Interacting Galaxy Pairs Using Identikit

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ABSTRACT
We develop and test an automated technique to model the dynamics of interacting galaxy pairs. We use Identikit (Barnes & Hibbard 2009; Barnes 2011) as a tool for modeling and matching the morphology and kinematics of the interacting pairs of equal-mass galaxies. In order to reduce the effect of subjective human judgement, we automate the selection of phase-space regions used to match simulations to data, and we explore how selection of these regions affects the random uncertainties of parameters in the best-fit model. In this work, we used an independent set of GADGET SPH simulations as input data, to determine the systematic bias in the measured encounter parameters based on the known initial conditions of these simulations. We tested both cold gas and young stellar components in the GADGET simulations to explore the effect of choosing HI vs. H$\alpha$ as the line of sight velocity tracer. We found that we can group the results into tests with good, fair, and poor convergence based on the distribution of parameters of models close to the best-fit model. For tests with good and fair convergence, we rule out large fractions of parameter space and recovered merger stage, eccentricity, viewing angle, and pericentric distance within 2$\sigma$ of the correct value. All of tests on gaseous component of prograde systems have either good or fair convergence. Retrograde systems and most of tests on young stars do not converge and may require constraints from regions other than the tidal tails and bridges.

Key words: galaxies: kinematics and dynamics, galaxies: interactions

1 INTRODUCTION
The merger of the galaxies and their associated dark matter halos is a fundamental process in galaxy evolution and cosmology. Galaxies and the dark matter halos they live in grow in time through mergers and accretion from the cosmic web. Over the past 8 billion years massive galaxies have transformed from disk star forming galaxies into inactive bulge-dominated ones (e.g. Bell et al. 2004; Faber et al. 2007). Galaxy mergers may be an important process that drives the assembly of galaxies, rapid star formation at early times, and the formation of bulge-dominated galaxies (e.g. Toomre & Toomre 1972; Mihos & Hernquist 1996; Barnes & Hernquist 1996).

Direct measurements of the initial orbital conditions of colliding galaxies are useful constraints for cosmology and galaxy evolution. Cosmological dark matter simulations predict hierarchical gravitational growth of structure with time. Numerical simulations predict the distribution of orbital parameters of dark matter halo mergers (e.g. Benson 2005; and Khochfar & Burkert 2006). If galaxies follow the dark matter halos, direct measurement of orbital parameters in galaxy mergers will put constraints on these simulations. In addition, idealized and cosmological zoom-in galaxy merger simulations have shown that merger induced star-formation history may depend on the initial orbital parameters of the interacting pair. (Cox et al. 2008; Snyder et al. 2011).

Moreover, integral field spectroscopy of nearby elliptical galaxies have shown that early-type galaxies in local universe can be categorized into fast and slow rotators (Cappellari et al. 2011; Krajnović et al. 2011; Emsellem et al. 2011). Recent results have shown that initial orbital parameters of major galaxy mergers can affect the rotational properties of their bulge-dominated remnants (e.g. see Bois et al. 2009; Bois et al. 2011; and Naab et al. 2014). Measuring these orbital parameters in early-stage mergers would make it possible to predict the kinematic properties of the merger remnant.

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Constraining the initial conditions of a pair of interacting galaxies is accomplished by finding a simulation reproducing both the morphology and kinematics of the data. (e.g. Toomre & Toomre 1972; White 1978; Barnes 1988). While some efforts have been made to model interacting galaxies by matching only the morphology (Toomre 1972; Shamir, Holincheck & Wallin 2013), line of sight velocity data is required to find unique dynamical models for many interacting systems (Barnes & Hibbard 2009). For example, the best-fit dynamical model for NGC 7252 (Borne & Richstone 1991) changed significantly when high quality HI kinematics data became available (Hibbard et al. 1994; Hibbard & Mihos 1995).

Barnes & Hibbard (2009) provides a review of the dynamical modeling of the interacting disc galaxies which have made use of kinematic information. These attempts have used different amounts of kinematic data; some have tried to match 2D kinematics obtained from HI or Hα maps (e.g. Hibbard & Mihos 1995; Duc et al. 2000; Struck et al. 2005), while others have only used 1D kinematics from long-slit spectroscopy (e.g. Mihos, Bothun & Richstone 1993; Díaz et al. 2000; Scharwächter et al. 2004). Most of these attempts rely on human expert judgment about the model that best matches the data. There has been some attempts to automate the matching process using genetic algorithms (e.g. Theis & Kohle 2001; Wahde & Donner 2001; Theis & Spinneker 2003). These algorithms have not yet matured enough to replace visual matching.

More kinematics information for modeling the dynamics of galaxy mergers will become available in near future with optical IFU and radio surveys providing large amounts of 2D line of sight velocity data for nearby galaxies. CALIFA (Sánchez et al. 2012), SAMI (Croom et al. 2012), and MaNGA (AS3/SDSSIV) are ongoing surveys of optical 2D spectroscopy of nearby galaxies including large numbers of interacting galaxy pairs. In addition, Australian SKA Pathfinder (Johnston et al. 2008) and MeerKAT (Booth et al. 2009) are going to be able to perform high resolution HI surveys of nearby universe. Thus, we need to develop robust tools to classify interacting galaxies based on this data.

Identikit is a tool for modeling major galaxy mergers (Barnes & Hibbard 2009; Barnes 2011). It combines self-consistent and test particle techniques in order to utilize fast exploration of the parameter space of a disc-disc encounter. In Identikit (Barnes & Hibbard 2009), the user can interactively change parameters like viewing direction and the orientation of the 2 disks until the best visual match between model and data is found. This interactive interface has been used for dynamical modeling of some major galaxy mergers (Privon et al. 2013). The visual match, though, is subjective and depends on user’s judgment about the most similar model. It requires a great deal of human-expert time spent on exploring the parameter space and looking for the best match. More importantly, the uncertainty in the initial conditions measured with Identikit 1 is not determined. Identikit 2, however, defines a quantity called “score” that provides an informal measure of the quality of the match. As a result, we can automatically search the parameter space and find the model with the maximum score, i.e. the best-fit model.

In this paper, we developed an automated routine based on Identikit 2. Our goal is to test the random and systematic uncertainties of modeling a major galaxy merger system using our method. In order to measure the systematics of Identikit modeling, we used GADGET SPH simulations (Cox et al. 2006; Cox et al. 2008) as input data. Because the initial conditions of the GADGET simulations are known we can measure the biases in the parameters of the best-fit model. We test both gas and young stars in the the GADGET simulations to compare the effect of choosing HI vs. Hα as the kinematics tracer. Using a statistical approach we also measure the random uncertainty of the best-fit model. In §2 and §3 we describe the methodology and the hydrodynamical simulations we use in this work. In §4 and §5 we present the results and discussion respectively.

2 METHOD

2.1 Identikit

Identikit (Barnes & Hibbard 2009; Barnes 2011) matches simulated disc-disc galaxy encounters to the observed morphology and kinematics of disc galaxy mergers. Assuming a particular mass model for the isolated galaxies (see §3.2), there are 3 groups of parameters describing the encounter of two disc galaxies. First are the orbit parameters which include eccentricity, pericentric distance, and mass ratio. Second are the parameters that describe the initial angular momenta of discs. The last group contains the parameters that depend on the observer’s time and location. The third group includes the viewing direction and the time of the merger as well as the parameters transforming the model to the physical scales of the real system (i.e. length/velocity scaling, and length/velocity offset). All of these make up 16 dynamical parameters involved in a disc-disc galaxy interaction. We list these parameters in Table 1.

The isolated galaxies consist of massive self-consistent and massless test particles with no dissipative (gaseous) component. The massive particles are distributed in a spherically symmetric fashion to represent the potential of a massive dark matter halo, a disc, and a bulge. The massless test particles, on the other hand, are distributed in discs with circular orbits. The motion of test particles is governed by the gravitational potential produced by massive particles. However, because they are massless, one may simulate test particles for multiple discs with different orientations simultaneously, without having them affect each other. As a result, one can calculate the trajectories of all possible disc particles in a single simulation run. In one run, the user obtains the morphology and kinematics of merger systems with discs of all different initial orientations. When comparing simulations to data, at each time step of the simulation, the user can turn on a particular disc and turn off the rest. Thus, Identikit quickly explores the parameter space in search for the best model.

Identikit can model the large scale morphology and kinematics of the tidal tails with a unique set of initial conditions. Early simulations of disc-disc galaxy mergers show that the shape and size of the tidal tails are sensitive to the initial conditions of the encounter (Toomre & Toomre 1972; Hibbard & Mihos 1995). These features move ballistically after the first passage and carry a memory of the initial conditions, and it’s been shown that there is little difference in
Table 1. List of Identikit parameters for a system of interacting galaxies. Barnes (2011) categorized these parameter into 3 classes. The number of degrees of freedom in each parameter is shown in the parentheses. As discussed in the text, we test 4 of these parameters, eccentricity, pericentric distance, time since pericenter, and velocity scale. For every Identikit model and for each value of velocity scaling Identikit 2 finds the best viewing angle and the best initial disc orientations by maximizing score. The rest of the parameters can be estimated from direct observations, independent of modeling. * The velocity scaling \( V \) relates the dimensionless velocity in Identikit to the physical velocity. If \( V_{\text{range}} \) is the velocity range in the Identikit velocity panels (top right and bottom left panels in Figure 1), the physical scale of unit velocity in Identikit, \( V_{\text{phy}} \), is \( V_{\text{range}}/(4 \times 10^2) \).

| Parameter Class            | Parameter                          | Range Tested                                        |
|----------------------------|------------------------------------|-----------------------------------------------------|
| orbital parameters         | eccentricity(1)                    | [0.60-1.10]                                         |
|                            | pericentric distance(1)            | [0.03125-1.0000] \( \times R_{\text{vir}} \)       |
|                            | mass ratio (1)                     | 1                                                   |
| observer dependent parameters | time since pericenter(1)          | from first pass to second pass                      |
|                            | viewing angle(2)                   | found through maximizing score in Identikit 2        |
|                            | position(2)                        | set by locking the centers                          |
|                            | length scaling \( L(1) \)         | set by viewing angle and locking the centers         |
|                            | velocity offset(1)                 | 0                                                   |
|                            | velocity scaling \( V(1) \)       | [-0.500-+0.500]*                                    |
| initial orientation of discs| (4)                                | found through maximizing score in Identikit 2        |

The primary advantage of Identikit’s test particle technique is rapid scanning of the multidimensional parameter space. Moreover, Identikit 2 quantifies the quality of the match, which is a unique feature. While visual matching is time consuming and subjective, providing a quantity (score) for the goodness of the fit is quantitative and requires less human expert time. However, massless test particles cannot reproduce self-gravitating features (e.g. spiral arms), and one cannot expect the dissipative features in gaseous components to be recovered. Tidal features are the key to recover a reasonable model. In some interacting galaxies such as retrograde ones, the tidal features are weak, and therefore they are more difficult to model. Also, score does not have an absolute significance like \( \chi^2 \). It is only useful for comparing quality of fit with the same set of boxes and cannot be used independently to determine the likelihood of the fit.

We create a library of Identikit models consisting of different time steps of simulations of galaxy mergers with varying orbital parameters. Each member of the this library is an individual frame with four fixed encounter parameters which we call external parameters (time, eccentricity, pericentric distance, and mass ratio). The user can study each member of the library in an interactive interface and explore other parameters of interest which include viewing direction, initial orientation of discs, length and velocity offsets, and length and velocity scalings. We call these internal parameters. Identikit 2 measures the score after the user locks the centers of model galaxies on the sky positions of the centers of the observed interacting galaxies. This constrains the position (length offset) and makes the viewing angle determine the length scaling \( L \) due to projection effect. So, locking the centers constrains two of the internal parameters. Identikit explores the viewing direction and the initial orientation of discs and finds the configuration that maximizes the score. So, for each member of the Identikit library at a particular velocity scaling and velocity offset, Identikit calculates a score.

In this work, merger systems consisting of two separate galaxies with distinct cores and strong tidal tails are examined. Identikit 2 can only be used to model separate galaxies. Additionally, by selecting galaxies which have not yet coalesced, we can independently estimate the mass ratio based on the measured light ratio. In this paper, we only study equal mass galaxy mergers. Additionally, tidal features are strongest during the time range between the first and the second passage. So, we restrict the current study to this time range. It may be possible to estimate a prior value for the velocity offset \( V \) by measuring the light- (mass-) weighted average (systemic) velocity of the merger system. Locking the centers constrains position and length scaling.

As a result, ignoring the freedom in choosing the mass model in isolated galaxies, we have six more encounter parameters to explore: eccentricity, pericentric distance, time (between the first and second passage), viewing angle, orientation of discs, and velocity scaling.

Of the remaining internal parameters, viewing angle and orientation of discs are determined when we maximize
Figure 1. Identikit model fit to a GADGET simulated data. The top left panels show the morphology, the bottom left and top right panels show the LOS velocity-position. The GADGET cold gas is shaded grey, and the best-fit Identikit galaxy models are the red and green points. Identikit uses the phase-space regions selected on the tidal tails (red and green boxes) to calculate the quality of the fit for each disc as functions of different viewing directions. Identikit calculates these functions at 80 viewing angles. The bottom right panel shows these functions as green and red shades on a spherical lattice. The best viewing direction is where the product of these functions is maximum.

score for each member of the library; however, velocity scaling is a free parameter. We can find the best score for each member of Identikit library with a fixed velocity scaling. So, we calculate score for models with a grid of parameter values for eccentricity, pericentric distance, time since pericenter, and velocity scaling. Initial orientation of discs and viewing angle (and therefore length scaling $L$) are determined independently when we calculate the score for each of these models. Table 1 shows the list of all parameters involved in Identikit and the range of the four parameters that are systematically explored in this work.

For an interacting system (i.e. a GADGET simulation in this work), one can make the map of scores of Identikit models with varying encounter parameters. In order to make such a map, we select a set of boxes on tides and bridges of the interacting system. Keeping the selected boxes fixed in place, we match all models in the Identikit library. For each member we change the velocity scaling as a free parameter and record how the score changes. Eventually, we obtain a score for all Identikit models with different eccentricity, pericentric distance, time, and velocity scaling. This makes an 4+1 dimensional scalar field. The model with the maximum score is the best-fit model. However, we still need to know how significant is the maximum score we found.

We perform a statistical evaluation to measure the uncertainty of the score for each Identikit model. We select the same number of boxes on the same tides and bridges but at slightly randomized positions. With the new set of boxes we calculate scores for all Identikit models again obtaining a new 4+1 dimensional score map. The new score map will have slightly different scores at each point in the parameter space. We repeat to make multiple score maps, each by moving the boxes around the tides and bridges of the interacting system. We calculate the average of the scores at each point in parameter space. Figure 3 shows a 2+1 dimensional slice of an average score map. Each cross represents an Identikit model with a particular set of parameters. The cyan box in Figure 3 shows the best-fit model with the highest average score, and the red box shows the input GADGET parameters. The contours show the models with scores that are within 1, 2, 3, and 4 standard deviation of the scores of the
best-fit model. We calculate the uncertainty in the best-fit parameters from these contours.

### 2.2 Box Selection

Even though Identikit 2 reduces the human subjective influence in finding the best match, it still depends on selection of box positions. If we move the boxes in X, Y, or V directions, or change their size or number, we select different regions of phase space. As a result, test particles populate them differently, leading to different scores. One position these boxes manually using an interactive interface in Identikit. In order to explore the effect of box selection and also to reduce the human interference, we developed a simple semi-automated routine for box selection. In this routine, boxes are selected akin prescribed user-selection in Identikit. Figure 2 describes our semi-automated routine.

Our automated box selection routine places the boxes on the tidal features and the bridges of the merger system. The algorithm attempts to place the boxes in the same manner as the manual selection of Barnes (2011). In this routine, first the segmentation maps of the system with different surface brightness levels are made. The surface brightness levels are manually adjusted to include faint tidal features in the segmentation map. In the next step, the user manually masks the central regions of the galaxies within the segmentation map, where he/she wants to avoid putting boxes. As explained earlier, Identikit reproduces the large scale tidal tails of the interacting galaxies, but not the self-gravitating details. So, boxes must cover not the centers of the galaxies. Finally, a user-defined number of boxes are randomly placed in the remaining region of the segmentation map (Figure 2).

The velocity of these boxes are determined by calculating the mass-(light)-averaged velocity of the gas (stars) inside the box. While there is still human influence in this routine (i.e. adjusting the surface brightness limit for segmentation map and masking the centers of galaxies), it is more automated than the original process in Identikit 2 and can be used for exploring the random effects of box selection. It should be mentioned that this routine only selects boxes of the same size, but Barnes (2011) often uses varying box sizes.

We have chosen the size of the boxes to be comparable to the spatial resolution of the data available. Here, we assume that the GADGET simulated galaxies are at the same distance as typical nearby major merger systems (e.g. the Mice galaxies). The HI data of nearby interacting galaxies have been obtained using VLA D and C arrays (e.g. Hibbard & van Gorkom 1996). The typical angular resolution of these observations is $\sim 20'' - 30''$ which is equivalent to $\sim 8 - 12$ kpc. For GADGET simulations of cold gas, we select the size of the boxes to be $\sim 6 - 8$ kpc. The optical $H_\alpha$ kinematics data obtained by many current instruments usually have a higher resolution. For instance, the diameter of the fibers in SparsePak on the WIYN telescope is $\sim 6''$, equivalent to $\sim 3$ kpc on a system like the Mice (Bershady et al. 2004). So, when testing the young stars in our simulations, we selected the boxes to be $\sim 3$ kpc.

The number of boxes also affects the scores because we select different phase space regions to be populated. For each test on GADGET simulations described in Figure 3 the number of boxes is fixed. We used a simple method to determine how many boxes to be used in each test. This method is the outcome of our initial trials. First, we obtain the maximum number of boxes that fit inside the allowed region (black region in Figure 2). Then, we take 2/3 of this as the number of boxes, unless this number is bigger that 22. This way, if the tidal tails are larger we select more boxes. The idea is that when the tidal features are more extended we have a stronger constraint. The limit of 22 boxes is because we noticed that when we use more than 22 boxes the results tend to have poorer convergence. We will describe convergence in § 2.2. As the size of the boxes is smaller in tests with the young stars, we have more boxes in these tests rather than the ones with cold gas. The range of number of boxes in the tests with gas is $\sim 8 - 16$ and in the tests with young stars is $\sim 13 - 22$. The number boxes used in each test is given in Table 2.

#### 2.3 Calculating Uncertainties in Best-Fit Parameters

The uncertainty of the best fit model is not given by Identikit itself. The results of our initial tests with Identikit showed that positioning the boxes is the largest source of uncertainty in the calculated scores. So, in order to get a measure of the uncertainty of the scores we move the boxes over the tidal tails and bridges of the data galaxy multiple times. More precisely, we use the semi-automated routine mentioned in § 2.2 10-100 times. Given each set of boxes, we measure scores for all Identikit models. The average and standard deviation of the scores is calculated for all models. The model with the highest average score is shown with the cyan box. The crosses enclose the models with scores within 1, 2, 3, and 4 times the standard deviation of the best-fit model. The crosses are also color coded with light gray showing higher scores and dark gray showing lower scores. It is important to remember that this figure shows a 2D slice of the score map showing scores for models with varying time and pericentric distance but fixed eccentricity (=1.0) and velocity scale (=0.1). The red square shows the known correct answer for the GADGET simulation which is almost on the 5 sigma counter.
Figure 2. Semi-automated box selection procedure: (a) Cold gas in a GADGET galaxy merger simulation (the fiducial model in test 1, see Table 2). (b) Segmentation map for two surface brightness levels. (c) The centers of the two galaxies are masked by the user to avoid selecting boxes in these regions. (d) We select 11 random points (boxes) in the remaining black region. The blue lines divide the regions for disc 1- (red), disc 2- (green), and overlap region (yellow) boxes.

of scores at each point in the parameter space is calculated. The model with the maximum average score is the best-fit model, and the models for which the average score is within 1, 2, 3, and 4 standard deviations from that of the best fit model are shown as the 1σ, 2σ, 3σ, and 4σ contours in Figure 3 respectively. Here, the standard deviation of scores at the best-fit model is used.

Because this is a computationally intensive job, we restrict the number of runs in which we move the box positions. To determine the number of runs we increase this number, and we can track how the 1σ and 5σ level contours change. We find at what approximate number these contours stop changing significantly with more runs. As can be seen in Figure 3, the contours do not change much after 10 runs in the test with cold gas. On the other hand, in the young star test there is a significant change between 10 and 100 runs. This may be due to the smaller box size and larger number of boxes used in young star tests (See §2.2). Based on this evidence, throughout this work we tested Identikit against the cold gas with 10 runs and against the young stars with 100 runs.

3 HYDRODYNAMICAL SIMULATIONS VS. IDENTIKIT

In addition to the random uncertainties we measure with the method described above, we can estimate the systematic biases in the best-fit model using an independent set of hydrodynamical simulations. We use the snapshots of the
Figure 4. The score map and standard deviation contours for matching (a) the gaseous component and (b) the young stars in a GADGET simulation. The solid contours are standard deviation for 10 runs and the dashed contours are for standard deviation for 100 runs. The standard deviation contours for the gas component do not change much from 10 runs to 100 runs, while the young star contours change significantly in this range. Throughout this work we use the standard deviation of 10 runs for gas tests and 100 runs for young star tests to calculate parameter uncertainties.

independent simulated systems as input data. Once we find the best-fit model, we can compare its parameters with the correct merger parameters of the simulation.

3.1 GADGET Simulations

We use smoothed particle hydrodynamical (SPH) GADGET-2 simulations of equal-mass disc-disc galaxy merger as input data (Cox et al. 2006 and Cox et al. 2008). The isolated galaxies are Sbc type galaxies with stellar and gaseous disc components and stellar bulge component, embedded in a massive dark matter halo. Each simulation follows a galaxy merger in a box of ∼ (200kpc)³. The spatial resolution is 100 pc, and the particle mass is ∼ 10^5 M⊙. The snapshots are available in 0.05 Gyr time steps. The simulations include radiative cooling, a density-dependent star formation recipe that reproduce Kennicutt-Schmidt relation (Kennicutt 1998), and a model to incorporate the effect of supernovae feedback and stellar winds. Even though feedback from active galactic nuclei (Di Matteo et al. 2008) is not included, these simulations capture more physical processes than simple test-particle Identikit models and are more realistic.

The mass models of isolated galaxies in GADGET simulations are different from Identikit models. Cox et al. (2006) and Barnes & Hibbard (2009) describe the mass models of the GADGET simulations and Identikit respectively. The halo concentration parameter is different between the two models (c = 11 in GADGET simulations and c = 4 in Identikit). The length scale that is used to match the two simulations is the scale radius of the NFW profile (Navarro, Frenk & White 1996). The stellar and gaseous disc scale length in the GADGET simulations is 4 kpc and 12 kpc respectively, which are 0.24 and 0.72 of the scale radius of the halo. In Identikit, isolated galaxies have a disc scale length that is 1/3 of the halo scale radius. We expect to see biases in the initial conditions of the matched simulations as a result of different mass models. However, in real world, the mass models of the interacting galaxies also differ from that of Identikit, and testing Identikit against a simulation with a different mass model helps us better understand the sensitivity of its results on the selected mass model for Identikit.

3.2 Model Details

We test Identikit against GADGET simulations described in Table 2. These models are selected to test the capability of Identikit in modeling systems with varying time since pericenter, viewing angles, eccentricity, pericentric distance, and initial disc orientations. We obtained these simulation via private communication with T.J. Cox, and the distribution of their initial parameters is not designed for the purpose of our tests. The fiducial GADGET simulation used in tests 1-6 is an equal-mass galaxy merger with parabolic orbit. The pericentric distance is equal to 11 kpc. In this simulation, both of the galaxies are prograde. In test 01 and test 02 we look at gas and young stars in a face-on snapshot midway between the first and the second passage. In most of other tests, all other parameters but one is similar to the tests 01 and 02. We investigate the isolated effect of varying each parameter on the systematic and random uncertainties of the best-fit. We examine cold gas (tests 01, 03, 05, 07, 10, 12, and 14) vs. young stars (tests 02, 04, 06, 08, 11, 13, and 15), merger stage (tests 03 and 04), viewing angle (tests 05 and 06), eccentricity (tests 07, 08, and 09), pericentric distance (test 09), and disk orientation (tests 10-15).
We can put a priori constraints on some of the encounter parameters by selecting interacting galaxies at certain stages of the encounter. Identikit 2 can only model merger systems with separate galaxies with distinct cores. In these systems we can estimate the merger mass ratio by measuring its light ratio. In addition, we are looking for galaxy merger systems that have strong tidal features which are the most pronounced after the first passage. We select to test GADGET Simulations at times long enough after their first pass and before their second pass, so that they are separate galaxies with strong tidal tails.

The hydrodynamical simulations have separate gaseous and stellar components, with distinguishable young and old stellar populations. For Identikit modeling, line of sight velocity information is required. This informations can be obtained from cold gas (e.g. HI 21 cm emission), ionized HII regions (e.g. Hα emission), molecular clouds (i.e. CO emission), or stars (absorption). Cold gas is usually more extended than the stellar population in galaxies. Resultingly, it shows more pronounced tidal features in galaxy mergers, and so it is expected to be easier to model with Identikit. However, obtaining high resolution HI data is more expensive than Hα emission line maps. In this work, we compare the result of Identikit modeling using cold gas (representing HI emission), vs. young stars (representing Hα emission from HII regions).

### 4 RESULTS

The primary output of the routine we described in §2 is a score map for each test in Table 2. The score maps are 4+1-
dimensional spaces (eccentricity, pericentric distance, time, velocity scale + score). As described in [21], each point in the score map refers to a member of the Identikit model library with a particular velocity scaling $V$. The viewing angle, orientation of discs, and length scaling $L$ is set by calculating the score for each Identikit model. The uncertainty of the scores at every point in the score map is obtained by measuring the scores 10-100 times, each with a new randomly selected set of boxes (§2.2), and calculating the average and standard deviation of scores at each point. The best matched Identikit model is expected to be that with the highest average score. This model is called the best-fit model and its parameters are the best-fit parameters. Models with average scores within $n$ standard deviations of that of the best-fit model are considered to be within $n\sigma$ of best-fit model. In order to visualize the variation of scores in the 4+1-D score map, we can look at the 2+1 dimensional slices of score map at the best-fit model and see the shape of the region with high score in different directions. As there are 6 ways to choose 2 parameters out of 4, we show six 2+1-D score maps in Figure 5. The extent of the $n\sigma$ contours in each of these four directions determines the uncertainty of the corresponding parameter.

In order to measure the uncertainty of the parameters of the best-fit model determined inside Identikit and not explicitly tested in the grid of models (i.e. viewing angle, orientation of discs, length scaling $L$, and physical time and physical $R_{peri}$ which depend on $L$), we study the distribution of model parameters with scores within the $1\sigma$ or $3\sigma$ contours in Figure 3. Figure 6 shows these distributions for test 01. Here the distribution of physical pericentric distance $(L/R_{peri}/R_{vir})$, physical time $(L/V \times T_{simulation})$, length scaling $L$, $\hat{n}_1 \hat{n}_2$ (dot product of orientation of the 2 discs), and $\hat{n}_i \hat{J}$ (dot product of the orientation of disc $i$ and system’s orbital angular momentum) are shown. The latter is a quantitative measure for the system being prograde vs. retrograde. When $\hat{n}_i \hat{J} = 1$ we have a prograde disc, when $\hat{n}_i \hat{J} = -1$ we have a retrograde disc, and when $\hat{n}_i \hat{J} = 0$ we have a polar disc. The correct parameter from GADGET simulation is shown with a dashed red vertical line so one can easily see the bias in the distribution. We use rose plots to show the distribution of angles in models within $1\sigma$ and $3\sigma$ contours. Figure 7a shows the rose plots for test 01. It includes the distribution of altitude ($\theta$) and azimuth ($\phi$) of the viewing direction, along with the inclination (i) andargument to periapsis ($\omega$) of each disc. The correct angles are shown with red dashed radial lines.

In some of the tests the $1\sigma$ distribution of initial orientation of discs converges into a narrow range of angles (Figure 7a). In these tests the models close to the best-fit model find close initial disc orientations, and we may infer that these models are small variations of the best-fit model. However, the $1\sigma$ distribution of initial orientation of discs can be wider for other tests, and in some cases this distribution is almost flat (Figure 7b). A wide or flat distribution indicates that the models with similar scores have very

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**Figure 5.** The average score maps of Identikit models matching to our fiducial GADGET simulation (Sbc201a, test 01). These are 2+1-D slices of the score map for varying (a) velocity scale and pericentric separation, (b) eccentricity and pericentric separation, (c) time and pericentric separation, (d) eccentricity and velocity scale, (e) time and velocity scale, and (f) time and eccentricity. These slices are taken at the best fit point which is shown by the red square. The color scale goes from best-fit (black) to 8σ from best fit (white). The red square shows the correct encounter parameters of the GADGET simulation.
different initial disc orientations, and there is a significant degeneracy in the best-fit model. In the most extreme case, when all disc orientations are equally likely we would find a cosine distribution in $\hat{n}_1, \hat{n}_2$ and $\hat{n}_i, \hat{J}$ histograms.

We categorize the results of our tests into three groups based on the distribution of $\hat{n}_i, \hat{J}$ in models within $1\sigma$ of the best-fit model. Tests with relatively narrow peak in $\hat{n}_i, \hat{J}$ distribution are “well-converged”. Tests in which the peak is considerably broader are “fairly-converged”. Finally, “poor” convergence is when we have an almost flat distribution in $\hat{n}_i, \hat{J}$. In order to quantify this categorization, we performed a KS test of the distribution of $\hat{n}_i, \hat{J}$ against a cosine function. Large KS test value means that the distribution is not a cosine function, and a small value means it is similar to a cosine function. When KS test value ($d_{KS}$) is bigger than 0.80 we call a good convergence. When it is less that 0.50 we take it as a poor convergence, and when it is between 0.50 and 0.80 we consider it as fair convergence. Note that KS test value limits are somewhat arbitrarily selected and can be changed to include more or less tests in good and fair groups. However, as can be seen in the best-fit vs. correct parameter plots later in this section, our selection of good, fair, and poor convergence is correlated with the accuracy of the results.

Five out of 15 tests in Table 2 had good convergence, three had fair convergence, and seven were poorly converged. All of the tests on gaseous components of prograde systems have good or fair convergence. The reason for poor convergence is either because Identikit can not find a configuration that populates the boxes, or it is because the boxes are not restrictive enough on orientation of discs and models with different orientations give similarly good scores. Five of poor converging tests are on the young stars in the GADGET simulation and four of them are on the retrograde systems. We will discuss this in 4.

4.1 The Fiducial Test

Figures 6 and 9 show the score map and distribution of parameters for test 01. This is a test on gaseous components of the the fiducial GADGET simulation (Sbc201a). The face-on snapshot is near the middle of the first and the second passages. Eccentricity and pericentric distance of the orbit is 1.0 and 11 kpc respectively, and both galaxies are prograde (one of them is completely prograde and the other one is tilted by 30 degrees). We identify this test as a good converging test because the KS test value for $\hat{n}_i, \hat{J}$ distribution against cosine function is bigger that 0.80.

As can be seen from Figure 5, our method rules out a significant fraction of parameter space in test 01. The scores of the Identikit models with correct eccentricity ($e=1$) are significantly higher than the models with incorrect eccentricity, making eccentricity measurement accurate ($\sigma = 0.03$) with no systematic bias. In this case $\sigma$ is set as the half of the increment in eccentricity of Identikit models used (grid size; see Table 1). The fractional time since pericenter is also well constrained. Fractional time since pericenter is the fraction of current time since pericenter to the total time between the first pass and the second pass. In this work, we chose most of the GADGET models in the mid-way between the

\[ \hat{n}_1, \hat{n}_2 = 0.7 \pm 0.1 \]
\[ d_{KS} = 0.90 \]
\[ \hat{J}, \hat{n}_1 = 0.8 \pm 0.1 \]
\[ d_{KS} = 0.90 \]
\[ \hat{J}, \hat{n}_2 = 0.8 \pm 0.2 \]
\[ d_{KS} = 0.81 \]
first pass and the second pass (i.e. fractional time \( \approx 0.5 \)). In this particular test the correct fractional time is 0.45. The obtained fractional time from Figure 6 is 0.49 \( \pm 0.09 \). This time is dimensionless, and in order to find the physical time since pericenter we need to scale it using the length and velocity scalings \( (L/V) \). The velocity scaling is one of the free parameters in our tests. However, as described in 3.1 length scaling is determined with viewing angle. So any bias in the measured viewing angle, leads to a bias in length scaling. The distribution of length scalings of the models within 1\( \sigma \) and 3\( \sigma \) contours are shown on the top-right panel of Figure 6. One can see that the length scaling is biased. However, the velocity scaling of models within the 1\( \sigma \) and 3\( \sigma \) contours is also biased in the opposite direction (Figure 5). So, distribution of physical time since pericenter for these models is not as much biased. (See top-middle panel of Figure 6). The measured physical time since pericenter is 0.59\( \pm 0.07 \) Gyrs, which is within 1\( \sigma \) of the correct answer (0.55 Gyrs). The orientation of discs with respect to orbital angular momentum is shown in \( \hat{n}_i, \hat{J} \) panels in Figure 6. For both discs the distribution correctly indicates prograde disc orientation. Correct answer is also recovered for viewing angles \( \theta \) and \( \phi \) in Figure 7a.

Black regions on the score maps of Figure 5 is broad in the direction of pericentric distance \( (0.38 R_{\text{vir}} \pm 0.17 R_{\text{vir}}) \). Nevertheless, the correct fractional pericentric separation 0.1643 \( R_{\text{vir}} \), is within 1.5\( \sigma \) of the best-fit value. In addition, the physical pericentric distance is obtained by scaling the dimensionless \( R_{\text{peri}} \), with the length scaling parameter \( L \). The distribution of physical pericentric distances is shown in the top-left panel of Figure 6. The average of this distribution is 18.1\( \pm 2.4 \) kpc. This is also within 3\( \sigma \) of the correct value, with a relatively smaller value for \( \sigma \).

We present the result of other tests by examining the parameters adjusted in the GADGET simulations in Table 2.

4.2 Time Since Pericenter

In tests 03 and 04 (see Table 2) we used the exact same GADGET model used in test 01, but observed at earlier and later fractional times respectively. Fractional time is the time since the first passage divided by the total time between the first and the second passages, so it is a measure of the merger stage. Test 03 is fairly converged with average \( d_{KS} = 0.61 \). In this test, the correct fractional time is 0.25, which is equivalent to 0.30 Gyr after the first pass. The obtained
fractional time for this model is $0.22_{-0.09}^{+0.17}$ and the measured physical time since pericenter is $0.42_{-0.38}^{+0.10}$ Gyr. Test 04 is well converged. In this test, the correct fractional time is 0.75, which is equivalent to 0.85 Gyrs after pericenter. The best-fit fractional time is $0.86_{-0.01}^{+0.02}$ and the obtained best-fit physical time is $0.96_{-0.10}^{+0.10}$ Gyr. Fractional time is biased especially in the later time test (test 04); however, it is encouraging that we recover the fractional time within 10% of the correct value.

In the rest of the tests we use snapshots of GADGET simulations that are near the middle of the first and the second passages (fractional time ~ 0.5). Figure 8 shows the best-fit vs. correct values of fractional time and physical time since pericenter. In this Figure we use different marker size, line thickness, and color darkness for tests with different convergence to make the good and fair ones look more prominent. We do the same for all best-fit vs. correct plots in this work. We only study tests with good and fair convergence. Parameters in tests with poor convergence usually have large uncertainties and are not reliable measurements. They are plotted, however, for the sake of comparison. In the tests on cold gas with good and fair convergence, there is an average bias of 0.1 toward later fractional times. The only test on young stars with fair convergence is also biased by less than 0.2 toward later fractional times. The physical time, which is obtained with a combination of length and velocity scalings ($L/V$), is more clearly biased toward later times (see Figure 15). For tests on cold gas the average bias is ~ 0.3 Gyrs, and for the test on young stars it is ~ 0.6 Gyrs. This systematic effect can be corrected when we apply our method on real data.

As we discussed earlier, the accuracy of results is correlated with KS test value, and the choice of KS test value limits to determine good, fair, and poor convergence is somewhat arbitrary. If we choose the limit for fair convergence to be 0.30, two other young star tests with KS test values of 0.39 and 0.33 (tests 08 and 11) will be included in the fair group. These two tests recover the fractional and physical time since pericenter similar to test 02 (i.e. with systematics of ~ 0.6 Gyrs). We can put meaningful constraints within 1σ on merger stage of these tests on young stars, even though their tidal tails are not as strong as in cold gas.

### 4.3 Eccentricity

Most of the GADGET simulations had eccentricity=1.0 (i.e. parabolic orbit). This corresponds to Keplerian orbits with zero energy, which is preferred if galaxies and dark matter halos they live in start approaching each other from stationary and gravitationally unbound origins. In all of the good and fair tests with eccentricity equal to 1.0, we recover the parabolic orbit of the interacting galaxies within 1σ. In Figure 9 which shows the measured eccentricity vs. correct eccentricity all of parabolic tests are on the black line, and their correct eccentricity is artificially slightly randomized to improve visibility.

In the tests with elliptical orbit, we recovered the elliptical nature of the orbit, though the eccentricity is underestimated. In tests 07 for which the correct eccentricity is 0.9, the measured eccentricity is $0.60_{-0.05}^{+0.15}$. In test 09 in which the correct eccentricity is 0.8 and the pericentric distance is larger than other tests, we also obtain an elliptical orbit, with 0.1 less eccentricity than the correct value ($e = 0.70_{-0.03}^{+0.11}$).

### 4.4 Pericentric Separation

Figure 10 shows the best-fit vs. correct answer for both the dimensionless ($R_{peri}/R_{vir}$) and physical pericentric distance. Identikit measures the pericentric separation in units of the virial radius of isolated galaxies which is the dimensionless pericentric distance. In order to find the physical pericentric distance one has to scale this dimensionless pericentric distance with the length scaling $L$. All but one of the GADGET simulations we tested have the same input $R_{peri}$ (11 kpc).

Fractional pericentric distance is within $3 \sigma$ of the correct value in all of well, and fairly converged tests (Figure 10). However when scaled with the length scaling $L$ to obtain the physical pericentric distance, they all move to
closely above the black line within $2\sigma$ (Figure 10b). Physical $R_{peri}$ in all of the good and fair tests is overestimated by $\sim 40\%$. This systematics can be corrected when we apply our method on real data.

4.5 Viewing Angle

Figure 11 shows the correct vs. obtained altitude in viewing angle. Most of the tests were face-on (Correct $\theta = 0^\circ$). Good and fair tests are scattered in the range from $-30^\circ$ to $+10^\circ$ degrees. From this plot it can be seen that there is not major difference between tests with gas and young stars when it comes to best-fit viewing direction of face-on systems.

Two of the tests (05 and 06) were on edge-on systems (Correct $\theta = 90^\circ$) with gas and young stars. The test with gas converged and the answer for $\theta$ of the viewing angle is within $20^\circ$ of the correct value. However, test 06 with young stars did not converge ($d_{KS} = 0.24$). We tried different box size and numbers to check if box positioning is the issue, but we were not successful in finding a good or fair converging answer. One possible reason is that the tidal tails are not well extended for the young stars in these GADGET simulations. Therefore, we have to put boxes near the center of the galaxies, and incorrect Identikit models with incorrect orientations and viewing directions can populate the boxes and get good scores. This causes a flat distribution in angles of models within $1\sigma$ or $3\sigma$ of the best-fit model similar to Figure 7b.

4.6 Initial Orientation of Discs

Figure 12 shows the correct vs. obtained values for orientation of discs in converged tests. We use $\hat{n}_i, \hat{J}$ to show the orientation of discs with respect to the orbital angular momentum of the galaxy merger. $\hat{n}_i$ is the unit vector of the orientation of disc $i$ and $\hat{J}$ is the unit vector of angular momentum of the orbit. So, when $\hat{n}_i, \hat{J} = 1$ we have a prograde disc, when $\hat{n}_i, \hat{J} = -1$ we have a retrograde disc, and when $\hat{n}_i, \hat{J} = 0$ we have a polar disc. Values in between these critical values reflect systems that are more or less prograde, polar, or retrograde. We also use $\hat{n}_1, \hat{n}_2$ to show the orientation of discs with respect to each other.

In prograde tests, the results are significantly different in gas and young stars. In all but one of galaxies in good and fair tests on cold gas the $\hat{n}_i, \hat{J}$ is within 0.5 of the correct answer. This is $\sim 90\%$ of the large and medium blue points in Figure 12a. About 70% of these points are within 0.2 of the correct answer. However, the tests with young stars are not as successful. Even the $\hat{n}_i, \hat{J}$ of the two galaxies in test 02 on young stars with fair convergence are not close to the correct value and have large uncertainties. The case is not any better for poorly converged tests.

All retrograde tests and the young stars in the polar test
had poor convergence. In tests 12 and 13 both galaxies were retrograde, while in tests 14 and 15, one was retrograde. In tests 10 and 11, one of the galaxies were on polar orbits. The cold gas polar test (test 10) had fair convergence. The measured uncertainty for $n_1, J$ is $\sim 0.5$ meaning that the orientation of discs are not well constrained in this test either. We expected poorer match for retrograde systems as the tidal features are less pronounced. However in original Identikit paper (Barnes & Hibbard 2009) some artificial merger models with retrograde discs were successfully reproduced by visual matching in the interactive interface of Identikit. This failure can be due to different reasons including the fact that the gaseous tidal tails in retrograde systems have an altered morphology compared with the stars, and that the tidal tails are even less strong when we study young stars. We will discuss these more in §.

5 DISCUSSION

Our method results in good and fair convergence in all of the prograde-prograde and prograde-polar tests on cold gas; nevertheless the retrograde tests and all but one of tests on young stars had poor convergence. In the converging tests, we can rule out a large fraction of the parameter space, albeit with systematic offsets from the input parameters. Time, eccentricity, pericentric distance, and viewing direction are better constrained than orientation of discs.

5.1 Parameters in Converged Tests

The random uncertainties are obtained by calculating how the scores are affected when we move the boxes around on tidal tails. In our early work on Identikit, we noticed that box positioning had the biggest effect on scores. Nevertheless, there may be other sources of random error (e.g. error from noise in the data) that we did not take into account in our calculations. So, the uncertainties we measured are lower limits to the real uncertainties.

Time since pericenter (both physical and fractional) is the best constrained parameter in tests with good and fair convergence. This is an important parameter as it is a measure of the merger stage, and tells us whether the interacting galaxies are in early or late stage. We selected the snapshots to be in the midway between the first and the second pass. But, in a couple of tests we recovered the time of an early and a late stage galaxy merger (see Figure 5). There is an average bias of $\sim 0.3$ Gyrs and $\sim 0.6$ Gyrs toward later physical times in tests on gas and young stars respectively. This bias could be due to the different mass models of the two simulations. The difference in the luminous to dark matter scale length affects the development of tidal features and the bridges. A more extended tidal feature may start to fall back into a galaxy earlier, making it look like a model with

![Figure 11. Correct vs. best-fit value of altitude of viewing angle. The blue markers are tests with gaseous component, and red markers are tests with young stars. The face-on tests are shown with circles and the edge-on test is shown with the triangle. Tests with good, fair, and poor convergence are shown with big, medium and small markers respectively. The correct values have been artificially scattered a little to make the points and error bars visible. The error bar of the test on the edge-on cold gas system is too small to be visible.](image1)

![Figure 12. Correct values vs. best-fit values of (a) $n_1, J$, and (b) $n_1, n_2$ for all GADGET models in this work. The blue markers are tests with gaseous component, and red markers are tests with young stars. The face-on tests are shown with circles and the edge-on tests are shown with triangles. Tests with good, fair, and poor convergence are shown with big, medium and small markers respectively. The correct values have been artificially scattered a little to make the points and error bars visible.](image2)
### Table 3.

List of measured parameters in each test. In tests 11, 13, and 15, we stopped after 50 runs because the test was not converging.

| Test ID | Component explored | Number of matching runs (KS test value) | Convergence quality | Best-fit pericentric distance | Best-fit eccentricity | Best-fit time to second pass |
|---------|--------------------|----------------------------------------|--------------------|-------------------------------|----------------------|----------------------------|
| 01      | gas                | 100                                    | good (0.85)        | 18.1 kpc (±0.4 kpc, ±0.04 R$_{vir}$) | 1.00 (±0.03) | 0.49 (±0.11) = 0.59 ± 0.07 Gyr |
| 02      | young stars        | 100                                    | fair (0.57)        | 13.2 kpc (±0.5 kpc, ±0.05 R$_{vir}$) | 1.00 (±0.03) | 0.67 (±0.05) = 0.93 ± 0.27 Gyr |
| 03      | gas                | 10                                     | fair (0.61)        | 30.3 kpc (±0.6 kpc, ±0.06 R$_{vir}$) | 1.00 (±0.03) | 0.22 (±0.17) = 0.42 ± 0.38 Gyr |
| 04      | gas                | 10                                     | good (0.86)        | 14.6 kpc (±0.8 kpc, ±0.08 R$_{vir}$) | 1.00 (±0.03) | 0.86 (±0.01) = 0.96 ± 0.10 Gyr |
| 05      | gas                | 100                                    | good (0.95)        | 15.9 kpc (±0.9 kpc, ±0.09 R$_{vir}$) | 1.00 (±0.03) | 0.42 (±0.10) = 0.70 ± 0.07 Gyr |
| 06      | young stars        | 100                                    | poor (0.24)        | 66.2 kpc (±3.2 kpc, ±0.3 R$_{vir}$) | 0.80 (±0.10) | 0.38 (±0.19) = 2.22 ± 2.5 Gyr |
| 07      | gas                | 10                                     | good (0.82)        | 25.2 kpc (±3.1 kpc, ±0.13 R$_{vir}$) | 0.60 (±0.05) | 0.58 (±0.01) = 0.36 ± 0.12 Gyr |
| 08      | young stars        | 10                                     | poor (0.39)        | 12.4 kpc (±0.4 kpc, ±0.13 R$_{vir}$) | 0.85 (±0.03) | 0.70 (±0.1) = 0.41 ± 0.06 Gyr |
| 09      | gas                | 10                                     | good (0.83)        | 64.1 kpc (±11.4 kpc, ±0.13 R$_{vir}$) | 0.5 R$_{vir}$ (±0.05) | 0.59 (±0.13) = 0.82 ± 0.21 Gyr |
| 10      | gas                | 10                                     | fair (0.54)        | 23.45 kpc (±0.7 kpc, ±0.05 R$_{vir}$) | 0.95 (±0.05) | 0.59 (±0.2) = 1.05 ± 0.37 Gyr |
| 11      | young stars        | 50                                     | poor (0.33)        | 60.87 kpc (±34.7 kpc, ±0.13 R$_{vir}$) | 0.95 (±0.03) | 0.59 (±0.13) = 1.56 ± 0.53 Gyr |
| 12      | gas                | 10                                     | poor (0.18)        | 66.20 kpc (±35.3 kpc, ±0.2 R$_{vir}$) | 0.75 R$_{vir}$ (±0.05) | 0.38 (±0.0) = 2.22 ± 2.1 Gyr |
| 13      | young stars        | 50                                     | poor (0.20)        | 50.77 kpc (±0.3 kpc, ±0.13 R$_{vir}$) | 0.5 R$_{vir}$ (±0.05) | 0.47 (±0.0) = 1.80 ± 1.53 Gyr |
| 14      | gas                | 10                                     | poor (0.16)        | 75.36 kpc (±9.9 kpc, ±0.13 R$_{vir}$) | 0.5 R$_{vir}$ (±0.05) | 0.50 (±0.0) = 3.07 ± 3.0 Gyr |
| 15      | young stars        | 50                                     | poor (0.43)        | 46.23 kpc (±35.6 kpc, ±0.03 R$_{vir}$) | 0.31 R$_{vir}$ (±0.02) | 0.30 (±0.01) = 1.12 ± 0.69 Gyr |
shorter tidal feature at a later time. Alternatively, this bias may be originating from the different nature of particles in GADGET simulations vs. Identikit. If the later is the main cause of the bias, we can correct for it when this method is applied on real data. With more tests on a variety of mass models we can track the cause of this bias more precisely.

Eccentricity, pericentric distance, and viewing angle are other parameters that are relatively well constrained. The tested GADGET simulations had limited range for these parameters, because we did not make them ourselves. All but one of the tests among the good and fair converged tests were face-on, and the measured viewing angle has been within $< 30^\circ$ of the correct value for all of them (See Figure 11).

Six out of 8 good and fair converging tests had parabolic orbit, and for all of them the eccentricity was correctly recovered, within 1σ. Based on this result, we are confident that our method worked well for eccentricity $e = 1$ orbits. We also recovered the elliptical nature of tests with eccentricity $e < 1$, though the eccentricity is underestimated by $\sim 0.1$-0.3. Physical pericentric distance is within 2σ of the correct value in all of tests with good and fair convergence. There is an average bias of $\sim 40\%$ toward larger physical $R_{peri}\,s$. Even when visual matching is utilized and the sophisticated patterns recognizable to human brain are matched, the pericentric separation is hard to model. The cause of the bias may also be the different mass models of the two simulations or because of using test-particles in Identikit.

The initial orientation of discs is not as well constrained. We will discuss the problems related to retrograde and polar galaxy mergers in the next sub-section. In well and fairly converged prograde tests on cold gas we are relatively successful in finding the correct orientation, $\hat{n}_i, \hat{J}$ in 90% of discs in tests with good and fair convergence is within 0.5 of the correct value, and 70% of these discs result in $\hat{n}_i, \hat{J}$ within 0.2 of the input value. However, $\hat{n}_i, \hat{J}$ is not well-constrained in tests with young stars (see Figure 12a).

Gas and young stars reveal significantly different results in terms of convergence. All prograde-prograde tests on cold gas have either good or fair convergence, while there is no good convergence in any of the young star tests, and only one of them is fairly converged. Of the parameters examined, time since pericenter and orientation of discs have significantly different results in cold gas vs. young stars. This is because young stars are less extended than cold gas, and the tidal features are not as strong (The disc scale length $R_d$ for gas is 3 times the $R_d$ for stars). Because young stars are a small portion of the total stellar population we expect that using data from all of the stars alleviate this problem. Nevertheless, measuring the kinematics of stars is more challenging in faint tidal features. In real data, young stars are traced by HII regions that emit Hα, a relatively easy-to-measure kinematic tracer. With optical and near infrared imaging we can measure the morphology of the total stellar population. We plan to do a few tests on the total stellar population in morphology and young stars in kinematics, to examine possible improvements in the results.

### 5.2 Poor-Convergence, Young Stars, and Retrograde Tests

In poor converging tests, Identikit results in random orientation for discs even in the models that are close to the best-fit model. So, when we plot the distribution of orientations in these models it looks similar to a uniform distribution in all possible directions (Figure 7b). Uniform distribution of orientations leads to a cosine distribution in $\hat{n}_i, \hat{J}$. In order to quantify convergence we perform a KS test on the distribution of $\hat{n}_i, \hat{J}$ against a cosine distribution. Small KS test value means that the distribution is similar to a cosine function and there is no convergence. On the other hand, from a large KS test value one may infer that the best models converged to a small range of possible orientations. A peculiar non-converging distribution (e.g. a distribution that has peaks near -1 and +1) can also give large KS test value against a cosine function, but we checked the results visually to make sure that there is no significant contamination from this type of non-converging distributions. In this work the KS test values of 0.80 and 0.50 are used as dividing values between good ($> 0.80$), fair($> 0.50$, $< 0.80$), and poor($< 0.50$) convergence.

The random orientation of discs can be the result of two scenarios. In some cases when Identikit does not find a good combination of orientation of discs and viewing angle that can populate the boxes, it gives score of -99.00 and arbitrary orientations for discs. Alternatively, one may place the boxes in certain regions, so that many disc orientations and viewing angles populate them equally well and result in good scores. Resultingly, the distribution of orientations will look similar to a uniform distribution. For retrograde and young star tests in this work it is likely that the second scenario is causing the non-convergence.

In most of the retrograde systems the tidal features are less extended and closer to the center of the system. This is also the case for young stellar components as opposed to cold gaseous components. The gaseous disc scale length is 3 times larger than that of the stellar disc in isolated galaxies of GADGET simulations. So the tidal features in the cold gaseous components are stronger. Our automated box selection routine selects boxes close to the center of the system with weak tidal features. The indicated phase space regions (boxes) can be populated with many configurations because of being close to the center of the galaxies. Models with poor visual match will obtain average scores that are as good as that of models with good visual match. So, the best-fit model and the models nearby will have a mix of parameters from well and poorly matched models, and this will make the distribution of orientations similar to that of a non-converging test.

For one of retrograde tests, we changed the size of the boxes and tried to place them manually (rather than using the automated routine) in places that are most similar to the choices in [Barnes 2011]. This attempt also failed. However, if we visually compare models with similar scores, we can distinguish a good match from a poor one. This means that Identikit algorithm does not capture all of the information one can possibly extract from visual matching. In order to improve Identikit we suggest to add a new type of box which may be called “penalty box”. We may put penalty boxes in phase space regions where no particles are present. If test-particles lay on these regions they may decrease the score of the corresponding model, which then may eventually exclude some of the visually poor matches, and partly break the degeneracy.

Retrograde mergers have other difficulties that make
their modeling more complicated. There is a significant difference in the shape and position of the tidal features when we study different components of the retrograde GADGET simulation. The gas is dissipative, and when gaseous arms collide, their position, velocity, and shape starts to offset from those of the stars. Since Identikit does not have a gaseous component, it does not reproduce these differences (Figure 13). Test particles better represent the stars, as they are collisionless. However, we are only testing young stars, which are a small fraction of all stars in these GADGET simulations. They are not extended as much as the total stellar population, and they have less similarity to Identikit models. One solution may be to match Identikit models to the total stellar population (Figure 13). However, measuring the stellar kinematics requires high signal to noise spectroscopy which is hard to obtain in faint tidal features. We plan to test total stellar population in morphology and young stars in kinematics simultaneously to see if we can obtain better results.

In general, it seems that tidal features are not sufficient to constrain the orientation of discs in retrograde disc mergers. It’s likely that using the information in the kinematics of the cores of the interacting galaxies would better constrain the initial orientation of discs. We plan to explore this more in future.

5.3 Summary

In this work we have developed an automated method for modeling pairs of interacting galaxies using Identikit. Our method measures the initial conditions of major galaxy mergers and provides the uncertainty for each measurement. We tested this method using an independent set of hydrodynamical simulations of encountering galaxies. We performed the tests on galaxy merger models with various encounter parameters in eccentricity, pericentric separation, time since pericenter, viewing angle, and initial orientation of discs. We also tested both gas and young stars in order to check the result of using different velocity tracers for kinematics data. We found that:

(i) We can group test results into good, fair, and poor convergence, based on the distribution of initial disc orientations in models within 1σ of the best fit model.

(ii) For all of the good and fair converged tests we recover the time since pericenter, eccentricity, pericentric distance, and viewing angle, within 30% of the range explored from the correct value.

(iii) The initial orientation of discs is constrained within 2σ for all good converged tests.

(iv) The tests performed on the cold gaseous components of GADGET simulations result in more converged and less biased initial conditions compared to the tests on young stars.

(v) We do not find acceptable convergence for any of the retrograde tests. All but one of the tests with young stars had poor convergence. This may be due to the fact that we only use the tidal features to find the best match, and tidal features are not as strong in retrograde systems or when we only study the young stars. The using of rotation curves as additional constraint on the system, and looking at the total stellar populations may improve these results. Besides, stripping or dissipation of gas may limit our tidal-tail finder.

Based on these results, our automated method can be used to find the initial conditions of prograde major galaxy mergers observed with HI emission line. However, we need to improve our modeling tool for retrograde systems with Hα kinematics data.

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