UV-Induced Mutagenesis in *Escherichia coli* SOS Response: A Quantitative Model

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*Abbreviations: NER, nucleotide excision repair; ssDNA, single-stranded DNA*

**Introduction**

The SOS response in the bacterium *E. coli* encompasses many proteins involved in detecting and repairing DNA damaged by a variety of agents, such as UV radiation, or chemicals such as mitomycin and bleomycin [1]. A complex regulatory network, comprising both transcriptional and post-translational regulators, controls the concentrations and levels of activity of these proteins (Figure 1).

The collective actions of this regulatory network are orchestrated so that the SOS response is commensurate with the magnitude of DNA damage [1]. Mutagenesis, such as the introduction of single-base substitutions in the DNA sequence, is not an inevitable consequence of DNA damage, but results from the action of specialized error-prone DNA polymerases that are part of the response [2]. This constitutes an extreme measure that might be useful for the cell only after very heavy DNA damage when DNA replication and repair cannot effectively proceed without it. While some mutations might benefit the offspring, the vast majority is nonmutagenic filling in of ssDNA gaps via homologous recombination [3], and it catalyses the cleavage of the transcriptional repressor LexA [6] and of the protein UmuD [7], whose cleaved form—UmuD'—is necessary for mutagenesis [1]. The drop in the level of the transcription factor LexA, due to its cleavage, de-represses the regulon involved in the SOS response. This regulon comprises about 30 genes, including those encoding the mutagenesis proteins UmuD and UmuC, RecA, and LexA itself. Also part of the SOS regulon are genes encoding UvrA, B, C—a group of nucleotide excision repair (NER) proteins that locate and excise damaged regions from the DNA [8,9].

Mutagenesis in UV-irradiated *E. coli* cells is mainly the direct result of the activity of the error-prone DNA polymerase, Pol V [2]. Pol V consists of two units of UmuD' and one unit of UmuC. It inserts several random base pairs in the DNA strand directly opposite a lesion, thus helping a replication fork to quickly bypass the lesion, after which Pol III can take over and continue replication. A distinct coordinated subnetwork of proteins centered on UmuD and UmuC controls the abundance, and thereby the activity, of Pol V (Figure 1).

Even though the SOS response in bacteria has been studied for several decades, new discoveries continue to be made. Recent single-cell experiments measured the temporal dependence of the activity of LexA-regulated promoters [10], which showed the following features: For low UV doses, the promoter activity peaks at about 10 min after the UV dose. This was also observed in bulk measurements of promoter activity averaged over a large population of cells [4] and can be attributed to the initial rapid drop in LexA levels after UV damage because of the activation of RecA,

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followed by a slow increase to its original level as the lesions are repaired by NER and the level of RecA* falls. More surprising was the observation that at higher doses of radiation, LexA-regulated promoter activity often had a second peak at about 30–40 min, sometimes even followed by a third peak at 60–90 min. This resurgence of the SOS response is puzzling because it indicates a temporary increase in RecA* levels at a time when the NER process is well under way and the number of lesions are already falling. This second peak (but not the third peak) was, however, absent in both ΔumuDC null-mutants and mutants that have an uncleavable version of UmuD (K97A) [10]. The common element in both types of mutants is the absence of Pol V, which suggests that the second peak is related to mutagenesis.

In this paper we propose a plausible mechanism for the appearance of this peak. We argue that E. coli bacteria can reliably measure the total amount of DNA damage. The ability of replication forks to bypass bulky lesions allows the cells to “count” the number of lesions they encountered over a fixed time interval (the average lifetime of RecA* filaments). The result of this count, given by the instantaneous number of RecA* filaments, is then fed into the mutagenesis regulatory subnetwork, which—as we show below—is designed to time-integrate this input signal over a long interval (30–40 min) and to abruptly turn on the Pol V if the integrated level of damage exceeds some critical threshold. The appearance of Pol V speeds up the bypass of lesions, and thus increases the rate at which new lesions are encountered by replication forks. We believe that this positive feedback from Pol V to the RecA* concentration is responsible for a temporary increase in the activity of SOS-regulated promoters 30–40 min after the radiation (the second peak reported in [10]).

**Results**

**Structure of the Model**

The goal of this paper is to model temporal dynamics of the mutagenesis subnetwork of the SOS response system (highlighted in yellow in Figure 1) for different doses and durations of UV radiation. This subnetwork is not isolated from the rest of SOS response, and therefore the model includes other parts of the entire E. coli regulatory network that interact with proteins involved in mutagenesis. Figure 1 shows the components of the SOS response that we quantify in our model. Different colored arrows correspond to different mechanisms of interactions between the nodes. An excellent earlier paper by Aksenov [11] contains a model of LexA-controlled transcriptional regulation coupled with the NER repair of lesions during the SOS response. Here that model is extended to incorporate the mutagenesis subnetwork. Full details of our model and parameter values are provided in the Methods section.

We mathematically model the temporal dynamics of the density of UV-induced lesions, as well as concentrations of LexA, RecA*, unbound UmuD, unbound UmuD’, UmuD–UmuD’ heterodimer, and Pol V, using a set of ordinary differential equations. Positive and negative terms in these equations represent different ways of production and consumption/degradation of the corresponding quantities. We do not explicitly simulate the creation and repair of individual lesions, nor do we simulate each replication fork moving along the DNA. Thus, our model ignores stochastic fluctuations. However, in later sections we do examine the effect of averaging over a population of cells in which various parameters, e.g., the number of replication forks, vary from cell to cell. This provides an in silico comparison between single-cell and cell-culture measurements. We also treat all time delays, such as when a replication fork is stalled at a lesion, in a simplified manner, i.e., we assume that these delays affect the RecA* level only via the average replication speed.

Most parameters in our model have been fixed using experimental data. For example, the experiments in [3,4,12] allow us to fix the RecA*-mediated cleavage rates of LexA and UmuD. The model has a total of 18 parameters of which only three could not be fixed by experimental data. We have therefore scanned a range of reasonable values for these three, as described in a later section.

Our model indicates four key features of the mutagenesis subnetwork in E. coli:

1. A mechanism for measuring the local amount of damage, coupling the number of RecA* filaments to the current lesion density.
2. A long-term “memory” used to time-integrate the RecA* signal and thus to determine whether the damage level remained high for a substantial time. This mechanism is based on slow accumulation of UmuD’.
3. Strong binding between UmuD and UmuD’, which provides a highly ultrasensitive increase in unbound UmuD’ levels as its concentration exceeds that of its “inhibitor” UmuD.
4. Positive feedback from Pol V to RecA* levels, which further increases the sharpness of the turn-on and turn-off of Pol V. This mechanism is also responsible for the second peak in activity of SOS promoters.

In the subsequent sections, we discuss each of the above aspects in more detail.

**Measuring Damage**

First we propose the following mechanism for the influence of the UV dose on the RecA* level. Consider a given replication fork proceeding on a DNA strand that has UV-induced lesions, as depicted in Figure 2. The Pol III DNA-polymerase stalls at the first lesion, generating an ssDNA gap that is then covered with RecA. This RecA filament exists for an average time, denoted $t_{RecA*}$, after which it disassembles. (We assume that each filament disassembles independently...
with a rate that is not limited by other DNA damage–induced processes.) During this time the replication fork may bypass the lesion and continue processing the DNA, leaving the first RecA filament behind. If the time the fork spends stalled at a lesion is sufficiently large or the lesion density is sufficiently small (so that the time the fork spends traveling between lesions is large), then the first filament will disassemble before the fork reaches the next lesion and creates another filament (as in Figure 2A). Therefore, in this case, there will be no more than one RecA filament per replication fork at any time. On the other hand, if the stall time is small or the lesion density is large, the fork will reach a second lesion before the first filament disassembles and, as a consequence, there may be many RecA filaments per fork existing simultaneously on the DNA (as in Figure 2B).

The RecA* level directly depends on the time a polymerase spends traveling between lesions, $s_{\text{moving}} = 1/v$, where $v$ is the average speed of the fork on undamaged DNA. For low lesion densities, the average concentration of RecA* also increases with the lesion density, its value being determined by the interplay between the stall time ($s_{\text{stalled}}$), distance between lesions ($1/\mu$), speed of the fork on undamaged DNA ($v$), and the RecA filament lifetime ($s_{\text{RecA}}$) (see main text).

**A. Lower lesion density ($\mu$ small)**

**B. Higher lesion density ($\mu$ large)**
DNA in a cell, i.e., $L_{\text{RecA}}^*$ expression multiplied by disassembly rate, i.e., any given time are such that the production rate equals the persistence time of a RecA* filament. Because the rates of filament production and disassembly speed with which Pol III processes DNA replication on undamaged DNA. This dependence can be quantified: one RecA* filament is produced every time the replication fork encounters a lesion. If the fork spends time $\tau_{\text{stalled}}$ at a lesion and time $\tau_{\text{moving}}$ between lesions, then the rate of production of RecA filaments is given by the following formula:

$$\text{filament production rate} = \frac{1}{\tau_{\text{stalled}} + \tau_{\text{moving}}}. $$

Further, the filament disassembly rate is $\tau_{\text{RecA}^*}$, where $N_{\text{fil}}$ is the number of RecA* filaments associated with the replication fork under consideration and $\tau_{\text{RecA}^*}$ is the average persistence time of a RecA* filament.

Because the rates of filament production and disassembly are much faster than all other processes we are interested in (the transcription of SOS genes and the rate of NER repair) [13], we can assume that the number of RecA* filaments at any given time are such that the production rate equals the disassembly rate, i.e.,

$$N_{\text{fil}} = \frac{\tau_{\text{RecA}^*}}{\tau_{\text{stalled}} + \tau_{\text{moving}}}. $$

The total amount of RecA*, $r^*$, is given by the above expression multiplied by $L_{\text{RecA}}^*$—the average length of a RecA* filament (taking into account the finite probability of forming a filament at each lesion a fork encounters)—and $N_{\text{fil}}$, the total number of replication forks currently digesting DNA in a cell, i.e.,

$$r^* = N_{\text{fil}}L_{\text{RecA}}^* = \frac{\tau_{\text{RecA}^*}}{\tau_{\text{stalled}} + \tau_{\text{moving}}}. $$

After fixing the parameter values based on experimental data (see Methods), this relation gives a RecA* level of approximately 100 nM for a fixed lesion density produced by a UV dose of $2 \text{ J/m}^2$, while it gives more than 400 nM for a UV dose of $50 \text{ J/m}^2$ (this neglects the effects of Pol V, which will be discussed later). The process shown in Figure 2 is thus a simple way for the cell to "count" the number of lesions on the DNA using a "memory," which is the finite existence time of a RecA filament.

**Accumulation and Heterodimerization of UmuD**

This is a short-time memory lasting only for a time $\tau_{\text{RecA}^*}$. However, the rate of UmuD* production is proportional to the amount of RecA*, therefore the UmuD* level is a measure of RecA* level integrated over time. Thus, UmuD* accumulates if damage (and therefore RecA*) persists for a long time. In our model, with RecA* at its maximum possible level, the timescale for the UmuD* level to exceed that of UmuD is about 15 min. For smaller UV doses, and therefore lower RecA*, this rise time can be more than 35 min. UmuD* is an integral component of the error-prone polymerase Pol V. However, UmuD* has to accumulate to a fairly high level before Pol V appears in any detectable quantities. The main reason for this is a strong physical interaction between UmuD and UmuD*. The binding between them is stronger than that between UmuD or UmuD* pairs; when UmuD and UmuD* are mixed in equimolar concentrations, the heterodimer is found to be much more abundant than either homodimer (UmuD–UmuD and UmuD*–UmuD*) [14]. This strong binding ensures that unbound UmuD homodimers required for Pol V formation appear in sufficient quantities only when (and if) the total concentration of UmuD* exceeds that of UmuD.

Figure 3 shows the equations we use to model the dynamics of UmuD, UmuD*, and Pol V. These equations model the following processes: (1) LexA repressed production of UmuD (highlighted in yellow), (2) RecA*–mediated cleavage of UmuD (highlighted in red), (3) heterodimerization of UmuD and UmuD* (highlighted in green), (4) degradation of UmuD* by ClpX when in the heterodimer, releasing UmuD (red), (5) dilution of all proteins due to cell growth/division (indicated by blue), and (6) formation of Pol V (green).

The Mutagenesis Subnetwork and Associated Dynamical Equations (Only Those Links Are Shown That Have Corresponding Terms in the Equations) $u$, $u'$, and $u_{\text{total}}$ are the concentrations of UmuD, UmuD*, and UmuD–UmuD* heterodimer, respectively, $r$ is the RecA* level, $l$ is the LexA level, $K_p$, $K_u$, $K_u'$, $c_{\text{Lex}}$, $K_{\text{L}}$, and $K_{\text{RecA}^*}$ are parameters (see Methods for their values). The equations describe (1) LexA repressed production of UmuD (highlighted in yellow), (2) RecA*–mediated cleavage of UmuD (highlighted in red), (3) heterodimerization of UmuD and UmuD* (highlighted in green), (4) degradation of UmuD* by ClpX when in the heterodimer, releasing UmuD (red), (5) dilution of all proteins due to cell growth/division (indicated by blue), and (6) formation of Pol V (green).
Here \( u_{\text{tot}} = u + u_{\text{hetd}} \) is the total concentration of noncleaved UmuD (in free or heterodimer form). The first term, \( \gamma_ur^r u_{\text{tot}} \), is the production of UmuD’ due to the cleavage of UmuD, the second term is the ClpX-dependent degradation of UmuD’ inside UmuD’–UmuD heterodimers, while the last term is the decrease in the concentration of UmuD’ due to cell growth and division (the dilution term) common for all proteins in the cell. With LexA and RecA* levels fixed, i.e., \( \gamma_{ur^r} \) constant, we can calculate the steady-state levels of UmuD and UmuD’ from these equations and, hence, the condition for Pol V to be present, i.e., when UmuD’ exceeds UmuD: \( u’_{\text{tot}} > u_{\text{tot}} \). Setting \( du’_{\text{tot}}/dt = 0 \) and minimizing the condition for \( u’_{\text{tot}} > u_{\text{tot}} \) we obtain the condition for \( u’_{\text{tot}} > u_{\text{tot}} \) in the steady state:

\[
\gamma_ur^r > \gamma_{dd^r} + \gamma_{dd^s}
\]

independent of UmuD production and degradation rates. Thus, Pol V abruptly appears once the Pol A level, and hence the value of \( \gamma_{ur^r} \), crosses and stays above the required threshold for long enough to allow UmuD’ to accumulate and pass the UmuD level. This analysis also suggests that there would be a threshold minimum UV dose below which Pol V does not appear because the NER repair brings down DNA damage quickly enough to bring the level of RecA* below the amount required to satisfy Equation 3.

Feedback from Pol V to RecA*

The behavior of replication forks at lesions (described above) naturally provides a positive feedback from Pol V to RecA* because Pol V reduces the stall time at the lesion, \( \tau_{\text{stalled}} \) ([2] estimates that Pol V bypasses lesions with 100- to 150-fold higher efficiency than Pol III). This is illustrated in Figure 4. Initially, there is no Pol V; however, other “nonmutagenic” translesion synthesis polymerases, Pol IV and Pol II (DinB or PolB), which are always present in the cell, ensure that even in the absence of Pol V the stalled replication fork could still bypass a lesion [18] at a rate we denote \( 1/\tau_{\text{stalled}}^{(0)} \). In Figure 4, this rate is slow enough that by the time the fork reaches the next lesion (after a time \( \tau_{\text{stalled}} + \tau_{\text{moving}} > \tau_{\text{RecA^*}} \), the first filament disassembles. At a later time, when Pol V appears, the stall time reduces dramatically [2,19]. The scenario depicted in Figure 4 assumes the bypass rate is dominated by Pol V-assisted bypass (for the more general treatment used in our model, see the Methods section). In this case, the reduction in stall time from \( \tau_{\text{stalled}}^{(0)} \) to \( \tau_{\text{stalled}} \) when Pol V appears is sufficient to allow the replication fork to reach a second lesion before the first RecA filament disassembles. Therefore, the RecA* level rises when Pol V appears. When this rise is fast enough, which occurs for a large enough UV dose, this results in a second peak in LexA-controlled promoter activities, as shown in Figure 5. Thus, the second peak is a natural consequence of the mechanism for setting RecA* levels represented by Equation 1. This prediction of the model is confirmed by the recent single-cell fluorescence experiments of Friedman et al. [10]. They also found that the second peak was washed out when the signal was averaged over many cells, probably because of cell-to-cell variations. Among the parameters, which can vary between cells, is the number of replication forks. We find that averaging the LexA-controlled promoter activity predicted by our model over many cells with differing numbers of replication forks produces a curve with a single peak (Figure 5, red dashed line) as observed in the experiments.

Tight Control of Pol V Levels

The model reveals an almost digital response of Pol V levels to UV, which provides very tight control of mutagenesis. Figure 6 shows the predictions of our model for the time course of Pol V (UmuD’–C) for different UV doses. In these simulations, the cell is subjected to an instantaneous pulse of UV at the specified dose at time zero. The main features of this plot are: (1) the existence of a UV dose (about 17 J/m²) below which the Pol V level is very low. Thus, with low damage, mutagenesis is virtually absent and DNA repair is error-free;
Below a threshold of about 17 J/m² there is no Pol V and, hence, no mutagenesis. The sharp onset of Pol V, in relation to both time and UV dose, is a direct consequence of the strong heterodimerization of UmuD–UmuD*. Thus, mutagenesis occurs only if the amount of UmuD–UmuD* exceeds that of UmuD, so that some free UmuD* is left to generate Pol V.

(2) a sharp onset in the generation of Pol V at about 15–35 min for UV doses larger than 17 J/m². The time of onset is largely UV-independent at high doses; (3) a rapid turn-off of Pol V at variable times that increase with the UV dose.

This plot confirms several points suggested by the analysis of the model in the previous sections. First, the existence of a minimum threshold UV dose below which no Pol V is produced is a consequence of the equations described in Figure 3 and, in particular, Equation 3. The rapid onset and the later rapid decrease of Pol V is due to the combination of heterodimerization and the previously described positive feedback from Pol V to RecA* levels. We provide more evidence to support this conclusion in the next section.

The Role of Association Strengths, Degradation, and Feedback on Onset and Turn-Off of Mutagenesis

The above analysis uses a simplifying assumption that the binding between UmuD and UmuD* is infinitely strong, so that the level of UmuD–UmuD* heterodimer is simply given by min([UmuD*], [UmuD]). The model can be used to examine the importance of the strength of this interaction in the mutagenesis response. Figure 7A illustrates the effect of decreasing this dissociation constant (K_{dd}). It shows that a strong association is critical in setting the abruptness and variable times that increase with the UV dose. However, feedback from Pol V to RecA* clearly, this feedback, combined with strong heterodimerization, is a crucial ingredient in the rapid onset of Pol V. Without feedback, the Pol V level is an order of magnitude lower compared with when there is feedback.

Saturation of RecA* and Peak Activity Levels

Another direct implication of Equation 1 is that the peak amount of RecA* saturates as the UV dose is increased. Indeed, as the density of lesions μ rises, \( \tau_{\text{moving}} = 1/\mu \) decreases. According to Equation 1, the RecA* level saturates once \( \tau_{\text{moving}} \) becomes much smaller than \( \tau_{\text{stalled}} \). Consequently, the height of the first peak of LexA-controlled promoter activity eventually saturates at high UV doses. During the second peak of promoter activity, the RecA* concentration rises again as \( \tau_{\text{stalled}} \) drops due to the Pol V–assisted bypass of lesions. The height of the second peak also saturates, but at higher UV doses. For the parameters used in our model, the amplitude of the first peak of promoter activity reaches 90% saturation around 25 J/m², while that of the second peak reaches it around 48 J/m² (see Figure 8B). This prediction of our model is in agreement with the experimental data in Figure 4C of [10], which show that the saturation of the second peak occurs at a higher UV dose than for the first peak. However, that data show the peak height averaged over a cell population. Therefore, to compare our model directly with the data, we show in Figure 8A the peak heights averaged more than 200 runs with varying \( N_f \). The result produces peak height versus UV dose curves match the data of [10] satisfactorily with the exception of the first peak data point at 50 J/m², which is lower than the previous data points. One explanation could be the ambiguity in the averaging procedure because, especially at higher UV doses, the second peak may sometimes be large enough to outswamp the first one, and hence be counted as a first peak, raising the red curve. Note, however, that at the single-cell level our model will always show a monotonically increasing peak height as UV dose is increased.

The behavior of our model also agrees with Figure 4A of [10] from which we conclude that the second peak of promoter activity starts to appear at a considerable frequency for UV doses between 10 and 20 J/m². The threshold of 17 J/m² predicted by our model (the same as the threshold for mutagenesis) is consistent with this.

The Response of the Cell to Continuous UV Damage

The SOS response of bacteria to radiation is typically studied by exposing them to a very short burst of UV light and then following the repair of the DNA damage. However, in environments for which bacteria are evolutionarily adapted, there may be both short bursts of the UV radiation, similar to the experimental conditions imposed on them, as well as much longer spells of low intensity UV exposure. The latter type of perturbation might not be well-suited for in vivo experiments but is easily achievable in our in silico model. Adding a new term representing a continuous low rate of production of lesions (see Methods) gives rise to a stable steady state wherein the rate of NER repair equals the rate of creation of the new DNA damage. Figure 9A shows the typical response to a continuous UV dose, which is low enough that mutagenesis is never triggered; LexA and RecA* take about 60 min to reach a steady state. Experiments in which cells were exposed to continuous UV damage because of the presence of a constant amount of mitomycin C also indicate
that the SOS response (rates of LexA repressor synthesis and cleavage) took 60 min to reach a steady state [3], confirming this prediction of our model.

We also simulated the response of our virtual cell to a pulse of UV radiation of a given integral intensity and duration that varied from 0 min to 300 min. Figure 9B separates the mutagenic and nonmutagenic regions of parameter space. Initially, the magnitude of the SOS response weakly increases with prolonging the duration of the pulse. This response was expected since very short pulses give the NER subsystem time to repair some lesions before replication forks encounter them; therefore, the average RecA* concentration is less than that for slightly longer pulses. The threshold for activating the mutagenesis subsystem reaches its minimum value for a 60-min pulse, and then it increases linearly throughout the duration of the pulse, indicating that the cell has reached the steady state in which mutagenesis is not triggered by the total intensity of the pulse, but rather by a sufficiently high rate of production of new lesions corresponding to a UV intensity per unit time of about 1.5 mW/m². This is an order of magnitude less than the typical solar UV intensity of 7–10 mW/m² in Copenhagen at noon on a clear day in December. For comparison, the solar UV intensity in the tropics in similar conditions is more than 100 mW/m² (see http://www.temis.nl/uvradiation/UVindex.html).

**Figure 7. Temporal Profile of Pol V Following a UV Dose of 20 J/m² as a Function of Various Parameters**

(A) The three curves refer, respectively, to strong (K_{diss} = 0.01 nM, blue), medium (K_{diss} = 1 nM, red), and weak (K_{diss} = 100 nM, black) binding between UmuD and UmuD².

(B) The effects of changing the binding constant between the UmuD² homodimer and UmuC: as binding strength 1/K in Equation 12 increases (K = 100, 10, 1 nM for the green, blue, and red curves, respectively), the Pol V concentration saturates at the 200 nM value set by the maximum cellular level of UmuC.

(C) For strong binding (K_{diss} = 0.01 nM), the three curves show the effect of increasing the degradation rate γ_{UmuD} of UmuD² by ClpX. As a default, the degradation rate is set equal to the dilution rate γ_{dil} (blue). The rate is half of the dilution rate for the red curve, whereas it is zero for the black curve. For the green curve, the degradation rate is double that of the dilution rate, which—at this level of UV damage—results in almost no Pol V.

(D) The effect of removing the Pol V to RecA* feedback. The blue curve is when there is feedback (as in Figure 7 A–C). The green curve is when there is no feedback, i.e., γ_{stalled} = γ_{stalled}(0), irrespective of the Pol V level.

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Discussion

When bacteria experience a large amount of DNA damage, their response has a mutagenic component that, it has been suggested, might afford some evolutionary advantage by altering the genome of offspring that would allow some of them to better survive high levels of the damage-inducing agents [20]. Precursors to an error-prone polymerase have also been implicated in slowing down DNA replication [21], thereby allowing additional time for accurate repair processes to remove lesions from the DNA. This delay is immediately terminated once the error-prone polymerases are fully formed. However, this kind of evolutionary strategy would be harmful where there was no damage, or when it was sufficiently low that it could be quickly repaired by error-free mechanisms. Hence, mutagenesis must be tightly regulated.

The main features of the mutagenic component of the SOS response system, according to published literature, are the following: (1) Mutagenesis is characterized by a sharp temporal onset and turn-off and threshold-like behavior as a function of UV dose. There is strong experimental evidence for this. For example, Rangarajan et al. [18] observed that in the absence of Pol II masking the effects, Pol V–assisted bypass rapidly appears about 45 min after the irradiation. Also, from Figure 4 of [21] we may conclude that the Pol V level crossing a specified threshold: 0.1 nM (yellow region), 1 nM (orange region), and 10 nM (brown region). (2) Mutagenesis gives saturated peak heights for increasing UV doses in our model as a consequence of Equation 3.

Figure 8. Saturation of Peak Promoter Activity at High UV Doses
(A) Height of the first (blue curve) and second (red curve) peaks in LexA–regulated promoter activity, averaged more than 200 runs each with a different value of \(N_f\), uniformly distributed between 1 and 3 (other parameters remained fixed as in Figure 4) as a function of the UV dose. Red circles and blue triangles show the corresponding data from Figure 4C of [10]. To facilitate comparison, the height of the red (blue) curve was normalized to match the maximum experimentally observed peak activity.

(B) The peak heights as a function of UV dose for a single run with \(N_f = 2\), with the same normalization as in (A). The saturation of peak heights for increasing UV doses in our model is a consequence of Equation 3.

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Figure 9. SOS Response to Prolonged UV Exposure
(A) LexA (blue) and RecA* (red) levels as a function of time in the presence of a continuous source of UV, which in 300 min (i.e., five cell generations) produces as many lesions as an instantaneous pulse of 20 J/m².

(B) The presence or absence of mutagenesis in our model in response to a pulse of UV radiation of a given integral intensity (y-axis) and duration (x-axis). Mutagenesis was detected in the colored regions. The criterion for its detection was the Pol V level crossing a specified threshold: 0.1 nM (yellow region), 1 nM (orange region), and 10 nM (brown region).

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rise to the second peak in activity of the SOS regulon. This is inferred from data in [10] that show this second peak is absent in mutants that lack UmuD or contain an uncleavable version of it.

We constructed a network model of mutagenesis in the bacterial SOS response system to account for these features. Figure 10 summarizes the key aspects of the behavior of the system that emerged in our simulations. We demonstrated that strong binding between UmuD and UmuD' is necessary for the sharp onset of mutagenesis and for its turn-off when UmuD' again falls below UmuD (see Figure 7A). Thus, initially, when levels of UmuD' are low, almost all of the UmuD' is sequestered in heterodimers so that no Pol V is generated. However, UmuD' is being constantly produced by the cleavage of UmuD, whose production, in turn, is elevated due to the de-repression of its promoter. If the UV damage is large enough, eventually the concentration of UmuD' rises sufficiently to exceed that of UmuD and allow the formation of Pol V. Additional control is afforded by the degradation of the UmuD–UmuD' heterodimer by ClpX, which removes UmuD' while freeing UmuD for further cleavage or dimerization. Although this degradation is not essential for the system's qualitative behavior, it substantially influences the turn-off time and rate (Figure 7B). Indeed, without it, turn-off could be only realized by the reduction in UmuD cleavage rates due to DNA repair and would depend solely on the slower NER mechanism. In addition, Lon actively degrades UmuD homodimers and UmuC [17]; its physiological advantages are unclear. Including this mechanism in our model does not affect the system's qualitative behavior, provided the degradation rate is not too large.

We suggested a simple mechanism by which the RecA* level can serve as a measure of the lesion density (see Equation 1). This mechanism relies on the possibility for RecA filaments to exist for some finite time after the replication fork has bypassed the lesion where the filament was created (note that we assume that this happens whether the lesion was on the leading or lagging strand). This allows the replication fork to sample a stretch of DNA, thus counting the damage density that is then manifested in the RecA* level. A direct implication of this mechanism is that there is a positive feedback from the Pol V to RecA* levels (see Figure 4). The resulting temporary increase in RecA* levels due to the sudden appearance of Pol V is sufficient to explain the resurgence of the SOS response 30–40 min after irradiation, observed in the single-cell experiments of Friedman et al. [10]. In addition, this mechanism also explains their observation of saturation of the peak promoter activities, and hence RecA* levels, upon increasing the UV dose (see Figure 8). Note that the first peak in promoter activity is produced due to changes in the lesion density, and thereby $\tau_{moving}$ as NER swings into action, while the second peak is due to changes in $\tau_{stalled}$, due to the action of Pol V. $\tau_{moving}$ and $\tau_{stalled}$ both affect RecA* level in the same way, being symmetrically placed in the denominator of Equation 1, but are influenced by different mechanisms.

Of course, various parameters that we use in our model will vary from cell to cell in a population. Such stochasticity plays an important role in the observed behavior, probably only for those components that are present in low numbers in the cell. Therefore, we consider that stochasticity in the number of replication forks is likely to be the most important source of cell-to-cell variability for the SOS system. As a default we take this number, $N_f$, to be 2. However, for comparing with data obtained from cell populations, we averaged several runs where $N_f$ was allowed to vary between 1

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**Figure 10. Summary of the Main Lessons of Our Model of the SOS Response and Mutagenesis**

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**Modeling Mutagenesis in E. coli**
and 3 (see Figures 4 and 8). Another component present in a relatively low concentration is UmuC, a variation of which is shown in Figure 7B. Figure 7C shows that the Pol V profile is quite sensitive to ClpX. Therefore, this might be another source of variability.

As more directly observable predictions of our model, we offer the following: (i) Overexpression of ClpX should considerably reduce the Pol V concentration. At the other extreme, the absence of ClpX would lead to Pol V being turned off at a later time than in wild-type cells (see Figure 7C). (ii) Overexpression of UmuC results in a flatter Pol V profile (see Figure 7B), while a UmuC mutant should not be able to produce Pol V and hence should behave like the ∆UmuDC and uncleavable UmuD mutants studied in [10]. (iii) We find that some overexpression of UmuD (up to a factor 2), or the introduction of more UmuD before the UV pulse, causes an increase in the second peak height. Further, the peak occurs earlier, sometimes even swamping the first peak. However, removing theLexA repression of UmuD (say by introducing UmuD on a plasmid with an unregulated promoter) results in the vanishing of the second peak, except at particularly high UV doses, because UmuD’ is not formed fast enough to cross the UmuD level.

There are alternative mechanisms by which UmuD and UmuD’ could affect LexA levels within the framework of the SOS model considered here. We discuss two mechanisms below that, unlike the mechanism we have concentrated on so far, could produce a second peak by causing a temporary rapid decrease of LexA, i.e., a trough in the average promoter activity profile.

(1) UmuD competes with LexA for the RecA* binding sites. Conceivably, high UmuD levels could prevent the access of LexA to them, thereby reducing its cleavage rate. This would create a trough (not a peak!) in LexA-controlled promoter activity at the peak of UmuD concentration. An important observation in [10] requires this mechanism of competition: peak LexA-controlled promoter activity in the ∆UmuDC mutant appears to increase with increasing UV dose (in the range 20–35 J/m²) rather than saturating, as in wild-type cells. Because of the absence of competition in the ∆UmuDC mutant, LexA is cleaved more and falls to a lower concentration than in wild-type cells, which, in turn, leads to a higher peak activity level of LexA-repressed promoters. However, if this competition is an important effect, the ∆UmuDC and uncleavable UmuD mutants studied in [10] should have different peak heights because the former would have no competition, while the latter should have more than wild-type (since the uncleavable UmuD K97A retains the ability to bind to the RecA filament [22]).

(2) UmuD was shown to preferentially bind to the beta-clamp subunit of DNA polymerase III while UmuD’ prefers to bind to the epsilon subunit [12]. Thus, by sequestering the beta-clamp, large levels of UmuD could possibly reduce the processivity of Pol III, which feeds back onto RecA* and LexA levels via \( \tau_{\text{stalled}} \) in Equation 1. Once again, the effect of this would be to produce a trough in LexA-controlled promoter activity. Later when the UmuD levels drop and the processivity of Pol II increases, it could lead to a second peak.

To explore these postulated causes of the second peak in RecA* levels, we incorporated each of these two feedback mechanisms into our model. In the absence of Pol V \( \rightarrow \tau_{\text{stalled}} \) feedback, these mechanisms, alone or in combination, did not generate the second peak in promoter activity at a reasonable time (within 40–50 min) after irradiation. However, their presence did not interfere with the manifestation of this feature when the Pol V \( \rightarrow \tau_{\text{stalled}} \) feedback was included in the model. Therefore, they might well be operating in parallel.

Friedman et al. also reported the existence of a third peak in the LexA-controlled promoter activities [10]. Unlike the second peak, the third one exhibited fewer fluctuations between individual cells. Indeed, its existence was previously mentioned in the Ronen et al. study, which used a signal averaged over many cells [23]. The generation of this third peak requires a mechanism that would increase the amount of RecA* at about 100–120 min after UV irradiation. As Friedman et al. suggest, one possible candidate is DinI, an SOS gene that is also repressed by LexA and induced in response to DNA damage. DinI is known to (a) stabilize already-formed RecA* filaments, (b) prevent RecA*-mediated cleavage of UmuD, and (c) leave the RecA*-mediated cleavage of LexA unaffected [22,24]. The first property would cause an increase in \( \tau_{\text{RecA*}} \) and thus if DinI were to be generated, or to become sufficiently active, about 100–120 min after the initial damage, it would result in a rise in RecA* levels and a new peak in LexA-dependent promoter activity. Yoshimatsu et al. [25] suggest that DinI coats RecA* filaments with a 1:1 stoichiometry. Therefore, its activity would become substantial only when its levels exceeded the RecA* levels in the cell. Since the RecA* levels are high (~7200 [4]) even in the absence of damage, and increase further due to de-repression of the SOS regulon, it might take up to 100–120 min until the induced DinI levels would overtake the diminishing levels of activated RecA*. This speculation is corroborated by co-IP results presented in Figure 2B of [26]. A plausible evolutionary role for such delayed RecA* stabilization is that it would support a stable low-level SOS response when the cell is exposed to a persistent source of DNA damage.

Overall, our model systematizes causes and effects in the best-known parts of the SOS response system in E. coli. It provides a framework for asking new questions about how (and why) the SOS response is organized. For instance, why is mutagenesis first initiated at such a late stage when only 10%–20% of the original lesions remain untouched by NER? One hypothesis would be that mutagenesis is triggered in response to the presence of particular types of lesions that are less efficiently bypassed by other mechanisms. This can be tested by extending the model to incorporate different kinds of lesions with different feedback to the stall time. Another key aspect is the length of the time window during which Pol V is active, which is set by the degradation times of UmuD, UmuD’, and UmuC. A more accurate determination of the regulation of these degradation times may shed light on effects of memory and why mutagenesis is at all initiated for severe DNA damage. In discussing this, however, one should keep in mind that mutagenesis may be designed to work primarily under a continuous source of DNA damage, and that the timing effects that we use to gain insight into the dynamics of the SOS response may be of secondary importance under typical real-world stresses. In any case, our study of the mutagenesis subnetwork suggests that its behavior is quite “digital,” in the sense that it makes a very quick transition from a state where there is no mutagenesis to a state where Pol V is fully activated.
Materials and Methods

The model. Our model of the SOS response defined by Equations 4–12, below, builds upon excellent earlier work by Aksenov [11]. Equations 4, 6, and 7 are very similar to their counterparts in [11], while Equations 5 and 8–12 are the new ones that we propose to describe mutagenesis and its feedback onto RecA* and LexA levels.

RecA-LexA feedback. The dynamics of LexA (l) level is modeled using the following equation:

\[
\frac{dl}{dt} = \frac{b_l}{1 + l/K_l} - \gamma_l l - \gamma_{gg} l\]

(4)

Here, the first term models the self-repression of LexA production. We assume a Hill coefficient of 1 [23]. The second term is for the cleavage of LexA by RecA* (whose level is denoted by l), while the third term is the degradation of LexA in non-irradiated cells.

The RecA* level (r), in turn, is described by:

\[
r^* = \frac{N_l L_{RecA} \tau_{RecA}}{\tau_{RecA} + \tau_{moving}}
\]

(5)

which is exactly the same as Equation 1 in the main text. In writing this equation for the RecA* level, we assume that the timescales involved in filament assembly and disassembly [13] are much smaller than those of transcriptional regulation and NER repair; therefore, a differential equation is not needed to describe the dynamics of RecA*.

Denoting the density of lesions by μ and the speed with which Pol III moves on undamaged DNA by v, we get the following expression for \(\tau_{moving}\):

\[
\tau_{moving} = \frac{1}{\mu v}
\]

(6)

The density of lesions is not a constant; they are continuously being repaired by the NER mechanism, which we model as follows:

\[
\frac{du}{dt} = -\lambda u.
\]

(7)

Here we assume that the repair is limited by the number of lesions and not by the Uvr proteins, hence the repair rate is proportional to the lesion density. In taking the rate of repair per lesion, \(\lambda\), to be a constant, we ignore the feedback from LexA to mRNA production of UvrC, which is not repressed by LexA.

Mutagenesis and the feedback from Pol V to RecA* and LexA. We can write the overall lesion bypass rate \(\frac{1}{\tau_{stalled}}\), as the sum of two rates, bypass due to Pol V (1/\(\tau_{stalled}^{(PolV)}\)), and bypass due to all other mechanisms (1/\(\tau_{stalled}^{(0)}\)).

\[
\frac{1}{\tau_{stalled}} = \frac{1}{\tau_{stalled}^{(0)}} + \frac{1}{\tau_{stalled}^{(PolV)}} \frac{P}{\text{K}_P + P}
\]

(8)

Here P is the Pol V level and \(P/(\text{K}_P + P)\) is the factor describing the concentration dependence of the Pol V-assisted bypass rate. This generalizes the situation described in Figure 4.

To describe the dynamics of the Pol V concentration, we must first consider concentrations of free UmuD (u), free UmuD’ (u’), and the UmuD-UmuD’ heterodimer uhetd:

\[
\frac{du}{dt} = \frac{b_u}{1 + u/K_u} - \gamma_u u + \gamma_{dd} u_{hetd} - k_{uw} u + k_{uw} u_{hetd} - \gamma_{dd} u
\]

(9)

\[
\frac{du’}{dt} = \gamma_u u’ [u + 2u_{hetd}] - k_{uw} u’ + k_{uw} u_{hetd} - \gamma_{dd} u’
\]

(10)

\[
\frac{du_{hetd}}{dt} = k_{uw} u - k_{uw} u_{hetd} - \gamma_{dd} u_{hetd}
\]

(11)

Finally, the Pol V level, which feeds back to RecA* and LexA levels via Equation 8, is given by

\[
P = \frac{Cu'^2}{K^2 + u'^2}
\]

(12)

These are the equations shown and explained in Figure 3.

Parameter values. Our model is fully specified by 18 parameters. Below we divide them into two groups, the first whose values we could fix directly or indirectly from published literature, the second for whose values there is inconclusive or no published data.

Parameters fixed from experimental data. (1) The repair rate by NER: \(\lambda = 0.035\ \text{min}^{-1}\), corresponding to a half-life of approximately 1 min as reported in [27] for cyclobutane pyrimidine dimers; (2) LexA concentration required for half-repression of LexA promoter: \(K_l = 270\ \text{nM}\), corresponding to an induction ratio of approximately 3.8 (the relation between the two is \(K_l = 1300(1 - l)\), where 1300 nM is the LexA level in undamaged cells [4]), interpolated from induction ratios of 6.7 and 4.8, measured at 30 °C and 42 °C, respectively [15]; (3) LexA concentration required for half-repression of UmuD promoter: \(K_u = 60\ \text{nM}\), corresponding to an induction ratio of approximately 22.7, interpolated from induction ratios of 28 and 17 measured at 30 °C and 42 °C, respectively [15]; (4) Dilution rate: \(\tau_{moving} = 0.012\ \text{min}^{-1}\), estimated average from a scatter plot of cell doubling time in [10]. Further, 60 min is the reported half-life of LexA in non-irradiated cells treated with chloramphenicol, i.e., in the absence of production of LexA [4], as well as from pulse-labeling measurements of LexA cleavage rates [3]. (5) Speed of Pol III on undamaged DNA: v = 1,000 bp s^{-1} [28]; (6) UmuC level; C = 200 nM [29]; (7) Number of lesions per unit UV dose: 50 per J/m². This corresponds to 250 lesions per E. coli genome for a dose of 5 J/m² [30]. Thus, for E. coli the initial lesion density is given by \(\mu = 0.22\ \text{min}^{-1}\times D\), where \(D\) is the UV dose in J/m². (8) Stall time in absence of Pol V: \(\tau_{stalled}^{(0)} = 0.22\ \text{min}\). In [10], the height of the first peak in LexA-repressed promoter activities reaches half-maximum at about 7–8 min. In our model, this occurs when \(\tau_{stalled}^{(0)} = \tau_{stalled}^{(PolV)}\). At 7–8 J/m², \(\mu = 7 - 8 \times 10^{-5}\ \text{min}^{-1}\) hence \(\tau_{moving} \approx 0.22\ \text{min}\) and \(\tau_{stalled}^{(0)} \approx \tau_{stalled}^{(PolV)}\) because the Pol V level is negligible. The chosen value is also consistent with an estimate of 10–12 s based on measurements of DNA synthesis in vitro in irradiated cells [30]. (9) Stall time in the presence of Pol V: \(\tau_{stalled}^{(PolV)} = 0.022\ \text{min}\). Tang et al. [2] estimate that Pol V bypasses lesions with 100- to 150-fold higher efficiency than Pol III. However, in vivo the ratio of \(\tau_{stalled}^{(0)} / \tau_{stalled}^{(PolV)}\) will be smaller than that because, apart from Pol III, other polymerases such as Pol II also contribute to the bypass rate [18]. Szekeres et al. [19] find that in ΑumuDC cells, the frequency of replication past cis-syn T–T dimers, produced by 4 J/m² irradiation, is approximately 40-times lower than when cells contain a chromosomal copy of ΑumuDC. In our simulations, we find that as long as \(\tau_{stalled}^{(PolV)} \gg \tau_{stalled}^{(0)}\), the dynamics do not depend much on the value of \(\tau_{stalled}^{(PolV)}\); therefore we conservatively chose \(\tau_{stalled}^{(PolV)} = 10\) (10) Parameter determining RecA* levels: \(N_l L_{RecA} R_{RecA*} = 110\ \text{nM}\) min⁻¹. (11) LexA cleavage rate (per nM of RecA*): \(\gamma_0 = 8.8 \times 10^{-4}\ \text{min}^{-1}\). These two parameters are together fixed so that the maximum rate of LexA degradation is \(N_l L_{RecA} R_{RecA*} \gamma_0 \approx 0.44\ \text{min}^{-1}\) corresponding to a half-life of about 1.5 min, chosen to match pulse-labeling measurements of LexA degradation rates in irradiated cells [3] and measurements in cells where LexA production was prevented by adding chloramphenicol [4]. Note that in our equations only the product of these two parameters, \(N_l L_{RecA} R_{RecA*} \gamma_0\), is relevant, so for the model simulations the individual value of each parameter is irrelevant as long as the product is preserved. However, we chose \(N_l L_{RecA} R_{RecA*} = 110\ \text{nM}\) min⁻¹ to fix the maximum possible RecA* level, to 500 nM. This is a reasonable number, obtained by assuming that \(N_l = 2\) and the maximum RecA* level is achieved when both these replication forks are stalled. Then, with each fork leaving an ssDNA gap of 900 nucleotides [11], and given that each RecA* filament has one monomer per 3–5 nucleotides [4,5], we obtain a maximum RecA* level about 750 nM. (12) UmuD-UmuD’ heterodimer uhetd level is fixed at \(1.8 \times 10^{-3}\) nM⁻¹ min⁻¹. This was chosen to be approximately five times slower than the LexA cleavage, estimated from the following data: After a UV dose of 20 J/m², the half-life of the UmuD to UmuD’ cleavage is approximately 45 min [12], while at the same UV dose, [4] reports a half-life for LexA of about 7–10 min. (13) Maximal LexA production rate: \(\beta_l = 86\ \text{nM}\) min⁻¹ (chosen so that in undamaged cells the level of LexA stabilizes to 1,300 nM [4], for which it must satisfy the formula \(\beta_l = 1,300 \times \gamma_l \times (1 + 1,300/\text{K}_l)\) (14) Maximum UmuD...
production rate: $\beta_s = 47$ nM min$^{-1}$ (chosen so that in undamaged cells the level of UmuD stabilizes to 180 nM [29] for which it must satisfy the formula $\beta_s = 180 \times \tau_{dd} \times (1 + (1.300/K_p))$) (15) Constant involved in concentration dependence of Pol V–dependent bypass: $K_p = 10$ nM. The level of Pol V in irradiated cells ranges from 15–60 molecules for small UV doses [31]. We chose $K_p$ such that this range of Pol V level would produce a substantial, but not saturating, contribution to $\tau_{dd}$. For parameters where data were unavailable or inconclusive, we have scanned a range of values around the following chosen defaults: (16) Binding constant of the UmuD–UmuD’ heterodimer: $K_{dhet} = 100$ nM, chosen to be very strong ($\beta_h$ and $\beta_r$ were individually chosen to be relatively large so that the heterodimer was, in practice, always in equilibrium with unbound UmuD and UmuD’). (17) Degradation of UmuD–UmuD’ by ClpX: $\tau_{dd} = 0.012$ min$^{-1}$. (18) UmuD’ level required for Pol V level to reach half maximum: $K = 10$ nM.

**Initial conditions.** For initial conditions, we have used the experimentally reported levels in wild-type cells: LexA = 1,300 nM [4], RecA* (naturally existing ssDNA, e.g., lagging strand replication gaps, does not activate RecA in the absence of DNA damage) [4], UmuD = 180 nM and UmuD’ = 0 [29].

The limit of strong heterodimerization. First, adding Equations 9 and 11, we get

$$\frac{d[u_{tot}]}{dt} = \frac{\beta_h}{1 + (K_u/K_p)} - \gamma_r \cdot u_{hetd} - \tau_{dd} \cdot u_{tot}.$$  

Here, $u_{tot} = u + u_{hetd}$ is the total amount of UmuD. Similarly, adding Equations 10 and 11 and using the fact that when heterodimer binding is infinitely strong, $u_{hetd} = \min(u_{tot}, u_{hetd} C^3)$, we get Equation 2 in the main text.

$$\frac{du_{hetd}}{dt} = \gamma_r \cdot u_{tot} - \gamma_r \cdot \min(u_{tot}, u_{hetd} C^3) - \tau_{dd} \cdot u_{tot}$$

Model of prolonged exposures to low-level UV radiation. To model the dynamics during exposures to pulses of UV radiation of finite (possibly long) duration, we modified Equation 7 as follows:

$$\frac{dP}{dt} = s - \lambda_P,$$

where $s$ is a source term, which is a nonzero constant when $0 \leq t \leq t_p$. Here, $t_p$ is the duration of the UV pulse and $s \times t_p$ is the total integral UV dose.

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