Convective Heat Transfer and Friction Factor Characteristics in Internally Threaded Tube with Constant Heat Flux for Al$_2$O$_3$/Water Nanofluid

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Abstract: This work presents an experimental study on the mean Nusselt number, friction factor and thermal enhancement factor characteristics in a circular plain tube and internally threaded tube under uniform wall heat flux boundary conditions for pure water and Al$_2$O$_3$ nanofluid as working fluid. The effects of the internal threads and nanofluid on the Nusselt number and the friction factor are determined in a circular tube with a fully developed turbulent flow for the Reynolds number in the range between 3000 and 25000. The horizontal tube with 1200 mm length was used as the test section having internal knuckle threads of pitch 12 mm. Firstly the experiments were performed on plain tube and internally threaded tube with pure water as working fluid and secondly with nanofluid consisted of Al$_2$O$_3$ nanoparticles with an average diameter of 12 nm dispersed in water having volume fraction of 1.5%. The heat transfer and pressure drop data obtained was compared with the data obtained from a plain tube under similar geometric and flow conditions. It is observed that at all Reynolds number, the Nusselt number and thermal performance increases for a tube with internal threads and nanofluid as compared with plain tube and pure water. These are because of increase in thermal diffusivity of nanofluid and also because of strength and intensity of vortices ejected from the internal threads. Subsequently an empirical correlation is also formulated to match with experimental results with ± 7% and ± 8%, variation respectively for Nusselt number and friction factor.

Keywords: Nanofluid, Internal threads, Turbulent flow and heat transfer characteristics.

1. Introduction

The convective heat transfer can be enhanced passively by changing the flow geometry, boundary conditions, or by enhancing the thermal conductivity of the fluid. Researchers tried to increase the heat transfer rate by increasing the thermal conductivity of the fluid. As a new research and technology frontier, nanofluids are used to enhance heat transfer. Nanofluids are engineered colloids which are made of a base fluid and nanoparticles (1-100) nm. The advantages of nanofluids are: (1) higher thermal conductivity than that predicted by currently available macroscopic models, (2) excellent stability, and (3) little penalty due to an enhancement in pressure drop and pipe wall erosion experienced by suspensions of micrometer or millimeter particles [1]. Such advantages of nanofluid offer important benefits for numerous applications in many fields such as petrochemical, refining, electronic, transportation, medicine, heating, and air-conditioning.

Fotukian and Esfahany [2] investigated experimentally turbulent convective heat transfer of dilute $\gamma$-Al$_2$O$_3$/water inside circular tubes. The nanofluid $\gamma$-Al$_2$O$_3$/water with dilute loading of 0.03 %, 0.054 %, 0.135 % were studied. The Reynolds number was varied from 6000 to 31000. The experimental results indicated that addition of small amount of nanoparticles to pure water improves the heat transfer performance significantly. The maximum value of 48 % increase in the heat transfer coefficient compared to pure water for 0.054 % volume concentration at Reynolds number of 10000 was observed. Increasing the particle concentration did not show much heat transfer enhancement in the turbulent region. The ratio of convective heat transfer coefficient of nanofluid to that of pure water decreases with the Reynolds number. The pressure drop of the nanofluid with 0.135 % volume concentration with showed 30 % increase at Reynolds number of 20000 compared to pure water.

Pak and Cho [3] studied experimentally the heat performance of Al$_2$O$_3$ and TiO$_2$ nanoparticles dispersed in water flowing in horizontal circular tube. Alumina and Titanium dioxide (TiO$_2$) nanoparticles with diameter 13 nm and 27 nm respectively were used in their study. They found that the Nusselt number of nanofluid increased with increases the Reynolds number as well as volume fraction. However they still found that the convective heat transfer coefficient of nanofluid with 3 % by vol nanoparticles was 12 % lower that of pure water at agaves Reynolds number. This may cause the nanofluid to have larger viscosity than that of pure water, especially at high particle volume fraction.

Hojjat et al. [4] investigated experimentally the forced convective heat transfer using dispersing $\gamma$-Al$_2$O$_3$, CuO, and TiO$_2$ nanoparticles in an aqueous solution of carboxymethyl cellulose (CMC). Their experimental apparatus included a uniformly heated circular tube under turbulent flow conditions passing through these nanofluids. Their results showed that the local and average heat transfer coefficients of nanofluids were larger than those of the base fluid. A new correlation was therefore proposed for the prediction of the Nusselt number of non-Newtonian nanofluids as a function of the Reynolds and the Prandtl numbers.
Yu et al. [5] measured the heat transfer rates in the turbulent flow of SiC/water nanofluid consisting of a volume concentration of 3.7% with 170 nm silicon carbide particles. Heat transfer coefficient increase of 50–60% above the base fluid water was obtained when compared on the basis of constant Reynolds number. Heat transfer mechanisms that involve particle interactions are believed for heat transfer enhancement.

Sajadi [6] investigated experimentally turbulent heat transfer behaviour of TiO$_2$/water nanofluid in a circular pipe with volume fraction of nanoparticles in the base fluid was in the range (0.05-0.25%) and Reynolds number range (5000-30000). The results indicated that addition of small amounts of nanoparticles to the base fluid augmented heat transfer remarkably. The measurements also showed that the pressure drop of nanofluid was slightly higher than that of the base fluid and increased with increasing the volume concentration. Experimental results have been compared with the existing correlations for nanofluid convective heat transfer coefficient in turbulent regime.

Another alternative method to enhance heat transfer is to insert twisted tape into a core tube. This approach induces secondary recirculation to the axial flow, leading to an increase in tangential and radial turbulent fluctuation and thus reducing a thickness of the boundary layer. Using nanofluid together with twisted tape for heat transfer enhancement was reported in numerous research works such as twisted tape inserts with Al$_2$O$_3$/water nanofluid [7] and [8], helical twist tape inserts with Al$_2$O$_3$/water nanofluid [9], twisted tape with alternate axis inserts with CuO/water nanofluid [10], twisted tape inserts with CuO/water nanofluid in corrugated tube [11], dual twisted tape inserts with CuO/water nanofluid in micro-fin tube [12], helical screw tape inserts with Al$_2$O$_3$/water nanofluids [13], helical screw tape inserts using CuO/water nanofluids [14], and propeller inserts with TiO$_2$/water nanofluid [15].

Heat transfer enhancement by inserting twisted tape is always escorted by the increase of flow resistance. The proper modification of twisted tape is a key approach to achieve a reasonable tradeoff between the increases of heat transfer rate and flow resistance. The driving force for this research work is to reduce the flow resistance due to these inserts by increasing the heat transfer rate. The aim of this study is to investigate experimentally flow and convective heat transfer characteristics of water-based nanofluid flowing through internally threaded tube of 35 mm inner diameter. The horizontal internally threaded tube with 1200 mm length is used as the test section.

2. Experimental Work

An experimental rig is built to study the convective heat transfer and flow characteristics of pure water and nanofluid flowing in a plain tube and internally threaded tube. The heat transfer test section is a straight brass tube with an inner diameter of 35 mm and a length of 1200 mm. Thermocouples are mounted at different places of the heat transfer test section to measure the wall temperatures and the fluid bulk temperatures. To obtain a constant heat-flux boundary condition, the heat transfer test section is heated electrically by a DC power supply capable of delivering a maximum of 3.5 kW. A Rotameter is used to measure the flow through the test section. The pressure drop of the heat transfer test tube is measured with manometer under an isothermal condition. The test section is isolated thermally from its upstream and downstream sections by plastic bushings to minimize the heat loss resulting from axial heat conduction. In order to minimize the heat loss from the test section to the ambient, the whole test section is thermally insulated. The hydrodynamic entry section is long enough to accomplish fully developed flow at the entrance of the heat transfer test section.

![Figure 1: Schematic diagram of the experimental apparatus](image1)

Firstly the experiments were performed on plain tube with pure water and Al$_2$O$_3$ water based nanofluid as working fluid. Secondly the experiments were performed on internally threaded tube with pure water and Al$_2$O$_3$ water based nanofluid as working fluid. The heat transfer and pressure drop data obtained was compared with the data obtained from a plain tube under similar geometric and flow conditions. The properties of fluids for the flow and heat transfer evaluations are based on the average temperature of tube wall and inlet–outlet fluid temperatures.

Before measuring the convective heat transfer coefficient of nanofluid, the experimental system was calibrated by comparing the measured Nusselt numbers of water at the fully developed turbulent flow with the calculated values using the Dittus-Boelter equation. The good coincidence between the experimental results and the calculated values shows that the precision of the experimental system is relatively high.
Thus, it can be concluded that the results from the present experimental facility are reliable. Thus, the facility was employed for further investigation with internal threads and nanofluid.

Data reduction
The data reduction of the measured results is summarized in the following procedures:

\[ T_s = \frac{(T_1 + T_2 + T_3 + T_4 + T_5 + T_6)}{6} \]

\[ T_b = \frac{(T_i + T_o)}{2} \]

Velocity of flow, \( V = \frac{Q}{A} \)

\( A = \) convective heat transfer area \((\Pi \times D \times L)\),
\( \frac{Re}{D} = \frac{\rho V D}{\mu} \)
\( D = \) inner diameter of pipe
\( L = \) Length of pipe
\( Q = Q_c + Q_r \)
\( Q = m \times C_p (T_1 - T_5) \)

\( Q_r = \sigma A \varepsilon (T_s^4 - T_b^4) \)

\( h = \frac{(Q - Q_r)}{(A (T_s - T_b))} \)

Experimental Nusselt number is calculated by

\( \text{Nu} = \frac{h D}{K} \)

Nusselt numbers calculated from the experimental data for plain tube were compared with the correlation recommended by Dittus-Boelter.

\( \text{Nu} = 0.023 \times \text{Re}^{0.8} \times \text{Pr}^{0.4} \)

Equation gives theoretical Nusselt number.

In straight pipe lengths, Pressure drop (\( \Delta P \)) can be calculated using the Darcy Equation

\[ \Delta P_{\text{Friction}} = \frac{f \times L_{\text{Pipe}}}{d_{\text{Pipe}}} \times \frac{\rho \times u^2}{2} \]

\( f = \) Darcy friction factor

Friction factor correlation

Correlation of Petukhov

\( f = (0.790 \ln(Re - 1.64))^2 \) for \( 3000 \leq Re \leq 5 \times 10^6 \)

3. Results and Discussions

Experimentally determined Nusselt number values for plain horizontal circular tube (without internal threads) with pure water as working fluid are compared with Dittus-Boelter correlation.

Fig. 3 shows the comparison between Nusselt numbers obtained experimentally and by using Dittus-Boelter equation for plain tube. It is observed that the value of \( \text{Nu} \) (experimental) is less than \( \text{Nu} \) (Dittus-Boelter). Actual heat carried away by water passing through the test section is the combination of convective and radiative heat transfers. As the heat transferred by convection alone is considered while performing experimental and numerical calculations, it can be expected that \( \text{Nu} \) (experimental) is less than \( \text{Nu} \) (Dittus-Boelter).

As shown in Figure 4 the Nusselt number increases with increases the Reynold number in pure water as well as in \( \text{Al}_2\text{O}_3 \) nanofluid solution. It can be clearly seen that the Nusselt number of \( \text{Al}_2\text{O}_3 \) nanofluid solution is higher than that of the pure water at a given Reynold number. The increase in Nusselt number is because of the fact that the he suspended \( \text{Al}_2\text{O}_3 \) nanoparticles increases the thermal conductivity of the two phase mixture. Furthermore, disorganized movement of these particles accelerated energy exchange process in the fluid. It is also observed that Nusselt number of \( \text{Al}_2\text{O}_3 \) nanofluid solution in threaded tube is higher than that of in plain tube. This is because of increase in swirling motion in threaded tube which in turn responsible for heat transfer enhancement.

![Figure 3: Comparison between the measured results and the calculated values of pure water in plain tube](image)

![Figure 4: Comparison Nusselt number of pure water and nanofluid solution as a function of Reynolds number in plain and threaded tube](image)

Figure 5 shows the pressure drop of pure water and \( \text{Al}_2\text{O}_3 \) nanofluid solution measured by pressure transducer. The pressure drop of the nanofluid is slightly increased compared with that of the pure water, because an increase in the friction loss is caused by suspension of \( \text{Al}_2\text{O}_3 \) nanoparticles in the pure fluid. On the other hand, pressure drop of \( \text{Al}_2\text{O}_3 \) nanofluid solution in threaded tube are greater than in circular tube. This phenomena is caused because of swirling motion created by threaded tube.
Figure 5: Pressure drop of pure water and nanofluid in plain and threaded tube

Figure 6 shows the variation of friction factor Vs Reynolds number pure water and Al₂O₃ nanofluid solution in plain and threaded tube. It is observed that the friction factor decreases with increase in Reynolds number for pure water and Al₂O₃ nanofluid solution in plain and threaded tube. The friction factor for nanofluid through threaded tube is more than that for plain tube. This is because of advancement in swirling motion due to artificial turbulence created by threaded tube.

4. Conclusion

The convective heat transfer and pressure drop characteristics that occur with internal threads and nanoparticles for a fluid flowing in a circular tube in the turbulent flow regime was experimentally investigated. The results are summarized follows:

- Convective heat transfer of the Al₂O₃–water nanofluid is significantly higher than those of the pure water.
- The pressure drop of the Al₂O₃–water nanofluid is approximately the same as those of pure water in the given conditions.
- The Pressure drop of internally threaded tube tends to increase slightly compared with plain tube.
- The convective heat transfer coefficient of the Al₂O₃–water nanofluid flowing in internally threaded tube increases by up to 21% compared with that of pure water flowing in a plain tube.
- The obtained results indicated that internal threads induced swirling-flow which played an important role in improving fluid mixing and heat transfer enhancement.

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