We present new limits on $\nu_\mu(\overline{\nu}_\tau) \to \nu_e(\overline{\nu}_\tau)$ and $\nu_e(\overline{\nu}_\tau) \to \nu_\mu$ oscillations by searching for $\nu_\mu$ disappearance in the high-energy wide-band CCFR neutrino beam. Sensitivity to $\nu_\tau$ appearance comes from $\tau$ decay modes in which a large fraction of the energy deposited is electromagnetic. The beam is composed primarily of $\nu_\mu(\overline{\nu}_\tau)$ but this analysis uses the 2.3% $\nu_e(\overline{\nu}_\tau)$ component of the beam. Electron neutrino energies range from 30 to 600 GeV and flight lengths vary from 0.9 km to 1.4 km. This limit improves the sensitivity of existing limits for $\nu_\mu \to \nu_\tau$ at high $\Delta m^2$ and obtains a lowest 90% confidence upper limit in $\sin^2 2\alpha$ of $9.9 \times 10^{-2}$ at $\Delta m^2 \sim 125$ eV$^2$.

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Neutrino oscillations occur if neutrinos have non-zero mass and mixing. If recent evidence for neutrino oscillations is confirmed, it will radically alter our understanding of both particle physics and cosmology. Neutrino oscillations may also explain the observed deficit of neutrinos from the sun. In the two-generation mixing formalism, the oscillation probability is given by

$$P(\nu_1 \to \nu_2) = \sin^2 2\alpha \sin^2 \left( \frac{1.27 \Delta m^2 L}{E_\nu} \right)$$

where $\Delta m^2$ is the mass squared difference of the mass eigenstates in eV$^2$, $\alpha$ is the mixing angle, $E_\nu$ is the incoming neutrino energy in GeV, and $L$ is the distance between the point of creation and detection in km.

While the high $\Delta m^2$ regions of parameter space for $\nu_\mu \to \nu_e$ and $\nu_\mu \to \nu_\tau$ oscillations have been excluded to very low mixing angles ($2 \times 10^{-3}$ for $\nu_\mu \to \nu_e$ and $5 \times 10^{-3}$ for $\nu_\mu \to \nu_\tau$) the high $\Delta m^2$ $\nu_e \to \nu_\tau$ parameter space is much less constrained as a result of the difficulty in producing high energy $\nu_\tau$ beams. The CCFR sample of over 20,000 charged-current $\nu_e$ interactions comprises the largest sample of high energy $\nu_e$'s to date. Previous high-statistics limits were obtained from reactor experiments with much lower beam energies. Accelerator limits were obtained by BEBC and Fermilab E531 which searched for $\nu_\tau$ appearance in emulsion.

We previously reported a limit on $\nu_\mu \to \nu_e$ oscillations by searching for $\nu_e$ appearance in the $\nu_e N$ charged-current data sample. In this report we present new limits using the same data sample on $\nu_e \to \nu_\tau$ and $\nu_e \to \nu_\mu$ oscillations. Both limits use a $\nu_e$ disappearance test. The $\nu_e \to \nu_\mu$ limit is also sensitive to $\nu_\mu$ appearance through $\tau$ decay modes in which a large fraction of the energy deposited is electromagnetic.

The CCFR detector consists of an 18 m long, 690 ton target calorimeter with a mean density of 4.2 g/cm$^3$, followed by an iron toroidal spectrometer. The target consists of 168 steel plates, each $3m \times 3m \times 5.15m$, instrumented with liquid scintillator counters placed every two steel plates and drift chambers spaced every four plates. The separation between scintillation counters corresponds to 6 radiation lengths, and the ratio of electromagnetic to hadronic response of the calorimeter is 1.05. The toroid spectrometer is not directly used in this analysis which is based on the shower profiles in the target-calorimeter.

The Fermilab Tevatron Quadrupole Triplet neutrino beam is created by decays of pions and kaons produced when 800 GeV protons hit a production target 1.4 km upstream of the neutrino detector. The resulting neutrino energy spectra for $\nu_\mu$, $\overline{\nu}_\mu$, $\nu_e$, and $\overline{\nu}_e$ are shown in Figure 3. The 2.3% $\nu_e$ component of the beam used in this analysis is produced mainly from $K^0 \to \pi^0 e^+ e^-$ occurring in the 0.5 km decay region just downstream of the production target. The $\nu_\tau$ content of the beam is less than $10^{-5}$.

Neutrino interactions observed in the detector can be divided into three classes depending on the type of incoming neutrino and interaction:

1. $\nu_\mu N \to \mu^+ X$ ($\nu_\mu$ charged-current (CC) events).
2. $\nu_{e,\mu}N \rightarrow \nu_{e,\mu}X$ ($\nu_{e,\mu}$ neutral-current (NC) events).

3. $\nu_eN \rightarrow eX$ ($\nu_e$ CC events).

The majority (97.7\%) of events observed in the detector are produced by muon neutrino interactions. The $\nu_\mu$ CC events can be identified by the presence of a muon in the final state which penetrates beyond the end of the hadron shower, depositing energy characteristic of a minimum ionizing particle in a large number of consecutive scintillation counters. Conversely, the electron produced in a $\nu_e$ CC event deposits energy in a few counters immediately downstream of the interaction vertex and is typically much shorter than the hadron shower. The separation of $\nu_{e,\mu}$ NC from the $\nu_e$ CC events is accomplished by using the difference in energy deposition pattern within the shower region; the $\nu_e$ CC events have a larger fraction of their energy deposited near the shower vertex.

In this analysis, the three most important experimental quantities calculated for each event are length, visible energy, and shower energy deposition profile. Event length is determined to be the number of scintillation counters spanned from the event vertex to the last counter with greater than a minimum-ionizing pulse height. The visible energy in the calorimeter, $E_{vis}$, is obtained by summing the energy deposited in scintillation counters from the interaction vertex to five counters beyond the end of the shower. The shower energy deposition profile is characterized by the ratio of the sum of the energy deposited in the first three scintillation counters to the total visible energy. Accordingly, we define

$$\eta_3 = 1 - \frac{E_1 + E_2 + E_3}{E_{vis}}$$  \hspace{1cm} (2)

where $E_i$ is the energy deposited in the $i^{th}$ scintillation counter downstream of the interaction vertex.

The event length is determined by the end of the hadron shower for $\nu_\mu$ NC and $\nu_e$ CC events but is determined by the muon track for most $\nu_\mu$ CC events. To isolate events without a muon track we parameterize the event length as a function of energy for which 99\% of hadron showers are contained as

$$L_{NC} = 4.0 + 3.81 \times \log(E_{vis}).$$  \hspace{1cm} (3)

Events which deposit energy over an interval less than $L_{NC}$ counters are classified as “short”, otherwise they are “long”. The long event sample consists almost exclusively of class 1 events, while the short sample is a mixture of class 2, class 3, and class 1 events with a low energy muon.

Events were selected with at least 30 GeV deposited in the target calorimeter to ensure complete trigger efficiency. Additionally, we require the event vertex to be at least five counters from the upstream end and more than $L_{NC} + 5$ counters from the downstream end of the target, and less than 127 cm from the detector center-line. The resulting data sample consists of 632338 long events and 291354 short events.

To directly compare the long and short events a muon track from the data was added to the short events to compensate for the absence of a muon in NC events. The fraction, $f$, of $\nu_\mu$ CC events with a low energy muon contained in the short sample (which will now contain two muon tracks) was determined from a Monte Carlo simulation to be approximately 20\%. A simulated sample of such events was obtained by choosing a long event with the appropriate energy distribution from the data and combining it with a second short muon track. The length of the short track and its angular distribution were obtained from a Monte Carlo sample of $\nu_\mu$ CC events.

A sample of $\nu_e$ CC interactions with a muon track added were obtained by convolving an electromagnetic shower generated using GEANT [10] with an event from the long data sample with the appropriate energy. This assumes $\nu_\mu - \nu_e$ universality. The energy distribution of $\nu_e$'s and the fractional energy transfer $y$ were obtained from Monte Carlo. Because the hadron showers in the long data sample already have a muon track, the $\nu_e$ CC sample can be compared directly with the short and long events.

The long and short $\eta_3$ distributions were further corrected by subtracting contamination due to cosmic ray events. The cosmic ray background was estimated from an event sample collected during a beam-off gate using an analysis procedure identical to the one used for the data gates. Additionally, the $\eta_3$ distribution of short $\nu_\mu$ CC events, normalized to the predicted fraction $f$, was subtracted from the short event sample. The $\eta_3$ distributions for short, long, and $\nu_e$ CC events for various energy bins are shown in Figure 3.

We extract the number of $\nu_e$ CC events in each of 15 $E_{vis}$ bins by fitting the corrected shape of the observed $\eta_3$...
The deficit in the measured value of $48.33$ to $78$ for $41$ degrees of freedom (DoF) with a mean oscillations. ($\nu$ shows the measured number of predicted by a detailed beamline simulation [14]. Figure 3. a no-oscillations assumption is $6$ this fraction we simulated charged-current interactions in which a large fraction of energy deposited this $\Delta$ data sample. These $\nu$ CC and long distributions are normalized to the respective number of events predicted by the fit.

distribution for the short sample to a linear combination of long and $\nu_e$ CC $\eta_3$ distributions:

$$\eta_3(\text{short}) = \alpha \eta_3(\text{long}) + \beta \eta_3(\nu_e CC) \quad (4)$$

The $\chi^2$ of the fit in each of the $15 E_{vis}$ bins ranges from $33$ to $78$ for $41$ degrees of freedom (DoF) with a mean value of $48$.

To search for $\nu_e$ oscillations the measured absolute flux of $\nu_e$’s at the detector was compared to the flux predicted by a detailed beamline simulation [14]. Figure 3 shows the measured number of $\nu_e$ CC’s for each energy bin compared with the predicted flux. The $\chi^2$ value with a no-oscillations assumption is $6.8/15$ DoF. We interpret a deficit in the measured $\nu_e$ flux as $\nu_e \to \nu_\tau$ (or $\nu_e \to \nu_\mu$) oscillations. ($\nu_e \to \nu_\mu$ oscillations are excluded above mixing angles of $2 \times 10^{-3}$ at the $90\%$ confidence level in this $\Delta m^2$ range).

If $\nu_e \to \nu_\tau$ oscillation occurs, some fraction, $f_e$, of $\nu_\tau$ charged-current interactions will be observed in our $\nu_e$ data sample. These $\nu_e$ CC-like events result from $\nu_\tau$ interactions in which a large fraction of energy deposited by the final state $\tau$ is electromagnetic. To determine this fraction we simulated charged-current $\nu_\tau$ interactions in our detector using GEANT and a combination of LUND [1] to generate charged-current neutrino interactions and TAUOLA [2] to simulate tau lepton decays. We fit the resulting $\nu_\tau$ charged-current Monte Carlo sample to a linear combination of pure $\nu_e$ CC and $\nu_e, \mu$ NC generated samples. The resulting $\nu_e$ CC-like fraction of $\nu_\tau$ CC events is $18\%$ for our data sample.

The effect of $\nu_e \to \nu_\tau$ oscillations on the observed $\nu_e$ spectrum was determined in the following way: a beamline simulation was used to tag the creation point of a $\nu_e$ along the decay pipe giving the survival probability for each $\nu_e$ as $(1 - P(\nu_e \to \nu_\tau))$ from Eq. (4). The predicted $\nu_e$ flux was normalized to the observed charged-current muon neutrino flux at the detector which was simulated in the same beamline Monte Carlo. We also added in the number of $\nu_\tau$ charged-current interactions which would appear in the extracted $\nu_e$ sample at the detector. The probability of observing a $\nu_\tau$ charged-current interaction in this data sample was calculated from the predicted normalized $\nu_e$ flux multiplied by the $\nu_\tau$ creation probability, $P(\nu_e \to \nu_\tau)$, and the $\nu_e$ CC-like fraction, $f_e$. We took into account effects of $\nu_\tau$ charged-current cross section suppression by including mass suppression terms [3], kinematic suppression for massive particle production, and the altered visible energy spectrum ($E_{vis}$) for $\nu_\tau$ charged-current events which contains visible energy from the tau decay in determining the effect of $\nu_\tau$ appearance.

The effect of $\nu_\mu \to \nu_\tau$ oscillations on the $\nu_e$ spectrum depends on the creation probability of $\nu_\tau$ from $\nu_\mu$, $P(\nu_\mu \to \nu_\tau)$. The $\nu_\tau$ appearance effect is calculated by multiplying $P(\nu_\mu \to \nu_\tau)$ by the $\nu_e$ CC-like fraction, $f_e$ and weighting by the $\nu_e$ CC cross section suppression factor. For completeness, we include a limit on $\nu_\mu \to \nu_\tau$ from this data sample (see Figure 3).

The major sources of uncertainties in the comparison

![Figure 2](image1.png)

FIG. 2. $\eta_3$ distributions for short (solid line), long (dashed line), and $\nu_e$ CC (dotted line) events in four of the energy bins studied. The $\nu_e$ CC and long distributions are normalized to the respective number of events predicted by the fit.

![Figure 3](image2.png)

FIG. 3. Number of electron neutrinos as a function of visible energy. For electron neutrinos the visible energy is equal to the total neutrino energy. The filled band shows Monte Carlo prediction assuming no oscillations. The curves shown are the effect of $\nu_e \to \nu_\tau$ oscillations for $\sin^2 2\alpha = 1$ and $\Delta m^2 = 150 \text{ eV}^2$ (dashed) and $\Delta m^2 = 10000 \text{ eV}^2$ (dotted).
of the $\nu_e$ flux extracted from the data to that predicted by the Monte Carlo are: the statistical error from the fit in $\nu_e$ flux extraction, error in shower shape modeling (described below), uncertainty in the absolute energy calibration of the detector (1%) which affects the relative neutrino flux extracted using a data sample with low hadron energy [13], and finally the uncertainty in the predicted flux of $\nu_e$'s at the detector which is estimated to be 4.1% [14]. This error is dominated by a 20% production uncertainty in the $K_L$ content of the secondary beam which produces 16% of the $\nu_e$ flux. The majority of the $\nu_e$ flux comes from $K^+\pi^-$ decays, which are well-constrained by the observed $\nu_\mu$ spectrum from $K^0\pi^0$ decays [14]. Other sources of systematic errors were also investigated and found to be small.

The uncertainty in shower shape modeling is estimated by extracting the $\nu_e$ flux using two definitions of $\eta$. Analogous to the definition of $\eta_3$ given in Eq. (3), we define $\eta_4$ to be the ratio of the sum of the energy deposited outside the first four scintillation counters to the total visible energy. If the modeling of the showers were correct, the difference in the number of electron neutrinos measured by the two methods should be small, any difference is used to estimate the systematic error. Since this error was shown not to be correlated among energy bins, we add it in quadrature to the statistical error from the fit.

The data are fit by forming a $\chi^2$ which incorporates the Monte Carlo generated effect of oscillations and terms with coefficients accounting for systematic uncertainties. A best fit $\sin^2 2\alpha$ is determined for each $\Delta m^2$ by minimizing the $\chi^2$ as a function of $\sin^2 2\alpha$ and these systematic coefficients. At all $\Delta m^2$, the data are consistent with no observed oscillations. Table I shows the best fit value of $\sin^2 2\alpha$ at each $\Delta m^2$ for $\nu_e \rightarrow \nu_\tau$ oscillations. The largest statistical significance of a best-fit oscillation at any $\Delta m^2$ is 1σ.

The frequentist approach [16] is used to set a 90% confidence upper limit for each $\Delta m^2$. The limit in $\sin^2 2\alpha$ corresponds to a shift of 1.64 units in $\chi^2$ from the minimum $\chi^2$ (at the best fit value in Table I). The 90% confidence upper limit is plotted in Figure 4 for $\nu_e \rightarrow \nu_\tau$ and $\nu_e \rightarrow \nu_\mu$. The best limits of $\sin^2 2\alpha$ are $<9.9 \times 10^{-2}$ is at $\Delta m^2 = 125$ eV$^2$ and $<8.3 \times 10^{-2}$ is at $\Delta m^2 = 125$ eV$^2$ respectively. For $\sin^2 2\alpha = 1$, $\Delta m^2 > 20$ eV$^2$ is excluded, and $\sin^2 2\alpha > 0.21$ for $\Delta m^2 \gg 1000$ eV$^2$ for $\nu_e \rightarrow \nu_\tau$.

As an alternative statistical treatment of this result we present 90% confidence limits based on the unified approach of Feldman and Cousins [17] recently adopted by the PDG [18]. Figure 12 shows all CCFR limits obtained using the longitudinal shower-shape method. Our previously published limit [8] on $\nu_\mu \rightarrow \nu_e$ used a one-sided confidence limit approach (as above).

In conclusion, we have used a high-statistics sample of $\nu_e$ charged-current interactions in the CCFR coarse-grained calorimetric detector to search for $\nu_e \rightarrow \nu_\tau$, $\nu_e \rightarrow \nu_\mu$ and $\nu_\mu \rightarrow \nu_e$ oscillations. We see a result consistent with no neutrino oscillations and find 90% confidence level excluded regions in $\sin^2 2\alpha - \Delta m^2$ phase space. This
FIG. 5. Excluded region of sin$^22\alpha$ and $\Delta m^2$ for (right to left) $\nu_e \rightarrow \nu_\tau$, $\nu_e \rightarrow \nu_\mu$ (disappearance), $\nu_\mu \rightarrow \nu_\tau$, and $\nu_\mu \rightarrow \nu_e$ (see Reference [7]) at 90% confidence using the Feldman-Cousins approach. The first three limits are new. The $\nu_\mu \rightarrow \nu_e$ limit differs from Reference [7] only in the construction of the 90% confidence limit.

result improves on existing limits for $\nu_e \rightarrow \nu_\tau$ in the range $50 \text{eV}^2 < \Delta m^2 < 200 \text{eV}^2$.

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