Pressure-induced structural transition, metallization, and topological superconductivity in PdSSe

Feng Xiao,1 Wen Lei,1,2 Wei Wang,1,3 Carmine Autieri,4 Xiaojun Zheng,1 Xing Ming,1,*, and Jianlin Luo5,6

1College of Science, MOE Key Laboratory of New Processing Technology for Nonferrous Metal and Materials, Guilin University of Technology, Guilin 541004, People’s Republic of China
2Key Laboratory of Artificial Micro- and Nano-Structures of Ministry of Education and School of Physics and Technology, Wuhan University, Wuhan 430072, People’s Republic of China
3School of Materials Science and Engineering, Beihang University, Beijing 100191, People’s Republic of China
4International Research Centre MagTop, Institute of Physics, Polish Academy of Sciences, Aleja Lotników 32/46, PL-02668 Warsaw, Poland
5Beijing National Laboratory for Condensed Matter Physics and Institute of Physics, Chinese Academy of Sciences, Beijing 100190, People’s Republic of China
6School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100190, People’s Republic of China

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Pressure not only provides a powerful way to tune the crystal structure of transition-metal dichalcogenides (TMDCs) but also promotes the discovery of exotic electronic states and intriguing phenomena. Structural transitions from the quasi-two-dimensional layered orthorhombic phase to three-dimensional cubic pyrite phase, metallization, and superconductivity under high pressure have been observed experimentally in TMDC materials PdS2 and PdSe2. We report a theoretical prediction of the pressure-induced evolutions of crystal structure and electronic structure of PdSSe, an isomorphous intermediate material of the orthorhombic PdS2 and PdSe2. A series of pressure-induced structural phase transitions from the layered orthorhombic structure into an intermediate phase and then to a cubic phase is revealed. The intermediate phase features the same structure symmetry as the ambient orthorhombic phase, except for drastic collapsed interlayer distances and striking changes of the coordination polyhedron. Furthermore, the structural phase transitions are accompanied by electronic structure variations from semiconductor to semimetal, which are attributed to bandwidth broadening and orbital-selective mechanisms. Specifically, the cubic phase PdSSe is distinct from the cubic PdS2 and PdSe2 materials by breaking inversion and mirror-plane symmetries but showing similar superconductivity under high pressure, which originates from strong electron-phonon coupling interactions concomitant with topologically nontrivial Weyl and high-fold fermions. The intricate interplay between lattice, charge, and orbital degrees of freedom as well as the topologically nontrivial states in these compounds will further stimulate wide interest to explore the exotic physics of the TMDC materials.

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I. INTRODUCTION

Since the discovery of atomic thin graphene, two-dimensional (2D) materials have received extensive attention [1,2]. As one important branch of 2D materials, transition-metal dichalcogenide (TMDC) materials have attracted more and more interest due to their superior electronic, optical, mechanical, and catalytic properties [3]. Layered TMDC materials $MX_2$ are commonly composed of quasi-2D $X-M-X$–type sandwich layers held together by weak van der Waals (vdW) forces, in which $M$ is the transition-metal element and $X$ is the chalcogen element such as S, Se, or Te. The bulk-phase $MX_2$ often crystallizes in the 1T polytype consisting of monolayer $MX_6$ octahedra, and the 2H and 3R polytypes with bilayer and trilayer stacked trigonal prismatic coordinated $MX_6$ layers [4]. As new members of the TMDC family, the noble-metal dichalcogenides (NMDCs) PdX2 materials are potential candidates for exotic physical properties and novel technical applications at the nanoscale [5–7]. Among them, PdTe2 tends to crystallize in a 1T structure with octahedral coordination [8,9], whereas PdS2 and PdSe2 adopt an unconventional orthorhombic structure named the 2O phase at ambient conditions, in which each Pd atom coordinates with four chalcogen atoms in a $(PdX_4)_2^{2-}$ square plane and resulting in a puckered pentagonal morphology [10,11]. Due to the strange pentagonal structure and unusual interlayer coupling interactions [12], the 2O phase PdS2 and PdSe2 materials host excellent physical-chemical properties and promising application prospects [5–7], including layer-dependent tunable band gaps [13–17], highly anisotropic properties [18–27], and ultrahigh air stability [17], which are promising materials for field-effect transistor [18,24], broadband photodetector [19,28,29], thermoelectric applications [13,21–23] and nonlinear photoelectronic devices [30].

Similar to conventional 2D semiconductors, the physical properties of PdS2 and PdSe2 are susceptible to external perturbations such as light [30], electric field [31], molecular adsorption [32], applied pressure [33–37], and strain [25,27,35,38–41]. Particularly, pressure and strain are two
Not only external stimuli but also internal factors such as vacancy defects [16,42–45], chemical doping [46–48], and surface oxidation [49] can be utilized to trigger structural transitions in PdSSe. Theoretical investigations show that the metallic electron structure originates from an orbital-selective mechanism [33,35]. High-pressure experiments reveal a dome-shaped relationship of the superconducting temperature with the pressure for the cubic pyrite phase PdS2 and PdSe2 [33,36]. Electronic structure calculations indicate that the superconductivity originates from strong electron-phonon coupling interactions combined with topological nodal-line states [35,36]. Meanwhile, excellent ferroelasticity with a low energy barrier and strong switching signal under strain has been theoretically predicted for PdS2 ferroelasticity with a low energy barrier and strong switching topological nodal-line states [35,36]. Furthermore, these ferroelastic transitions accompanied with crystal orientation rotations give rise to tunable transport properties and switchable thermal conductivity [25,27,35,40].

Not only external stimuli but also internal factors such as vacancy defects [16,42–45], chemical doping [46–48], and surface oxidation [49] can be utilized to trigger structural transitions and manipulate the physical-chemical properties of PdS2 and PdSe2. Experiments demonstrate that plasma irradiation [42] or electron irradiation [44] can induce Se atom vacancy in PdSe2, which breaks the Se-Se dumbbell-shaped dimers and results in huge structural distortions and formation of metallic Pd17Se15 and novel 2D Pd2Se3 materials [42,44]. The defect states in PdSe2 can be reversibly switched between charge neutral and charge negative and show anisotropic carrier mobility [43,45]. First-principles theoretical investigations show that hole doping can induce half-metallic ferromagnetism in the PdSe2 monolayer, and the magnetization direction can be controlled by a transverse uniaxial stress [48]. Furthermore, controllable partial oxidation of the surface of PdSe2 by ozone treatment successfully modifies its transport property, optoelectronic performance, and catalytic activity [49]. On the other hand, due to the different ionic radii, doping or substitution can induce chemical pressure in crystals, which are considered as specific methods conducive to stabilizing pressure-induced superconductivity or other characteristic phenomena at ambient conditions [50]. Recently, Te substitution-induced structural evolutions from the orthorhombic 2O phase to a monoclinic verbeekite phase and then to a trigonal IT phase are observed in the PdSe2–xTe x system, accompanied by a drastic change of the electrical transport behavior from semiconductor to metal and enhanced superconductivity with increasing Te content [46,51]. In addition, a solid solution of PdSe2–xS x with a wide range of x (0 ≤ x ≤ 0.86) has been synthesized by atomic substitution, which shows tunable density of states, effective mass, and band gap by changing x [47].

Although 2O-phase PdSSe, an isomorphous intermediate material of orthorhombic PdS2 and PdSe2, has been synthesized for over half a century [11], its detailed crystal structure is only reported by our theoretical works recently [52]. As shown in Fig. 1, the bulk phase of PdSSe is constituted by two types of monolayer PdSSe (denoted as A and B) and forms three polymorphs with different stacking manners (denoted as AA, AB, and BB). Previous theoretical predictions indicate that PdSSe will exhibit intriguing properties, including excellent photocatalytic properties and tunable band gap under biaxial strain, which are promising characteristics for high-performance optoelectronic, nanoelectronic, photovoltaic, and photocatalytic applications [52,53]. Although tremendous focus has been paid to PdS2 and PdSe2, the study on their counterpart PdSSe is scarce. Considering that PdS2 and PdSe2 are featured with rich phase transitions, tunable properties, and interesting superconducting behavior under stress or pressure [25,27,33–41], one may naturally expect similar behavior to be observed in their sister material PdSSe. In the present work we explored the structural evolutions of the bulk-phase PdSSe under hydrostatic pressure, uncovered an electronic structure transition from semiconductor to semimetal and superconductor, revealed the origin of the metallization, and predicted topological superconductivity for the high-pressure phase. The predicted structural transitions and unconventional transport properties concomitant with topologically nontrivial states in PdSSe supply a meaningful complement to the hectic NMDC materials of PdS2 and PdSe2, which will attract extensive interest from a wide audience to explore its unanticipated properties.
II. CALCULATION METHODS

Geometry optimization and electronic structure calculations were performed by using the Vienna Ab initio Simulation Package (VASP) [54,55] based on the density functional theory. The projector-augmented-wave potential, the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional [56], and the plane-wave basis set with a cut-off energy of 520 eV were employed. The smallest allowed spacing of the reciprocal space between \( k \) points was fixed to 0.2 Å\(^{-1}\). In order to obtain a more accurate band gap close to the experimental value, the Heyd-Scuseria-Ernzerhof (HSE06) [57,58] hybrid density functional was adopted to calculate the band structures. Electron-phonon interaction calculations were performed by the density functional perturbation theory with the QUANTUM ESPRESSO (QE) code [59]. Electron-phonon coupling constants were calculated on phonon and electron grids of \( 4 \times 4 \times 4 \) and \( 16 \times 16 \times 16 \), respectively, with a Gaussian smearing width of 0.05 Ry, and the plane-wave cut-off energy was set to 50 Ry for all three polymorphs of PdSSe. As shown in Fig. S1 in the Supplemental Material (SM) [60], the convergence tests of energy cutoff and sampling of \( k \) points demonstrated the parameters employed in the present work were convincing and accurate enough.

The electron-phonon coupling constant \( \lambda \) and the superconducting transition temperature \( T_c \) for PdSSe are calculated by the Allen-Dynes-modified McMillan formula [61,62]:

\[
T_c = \frac{\omega_{\text{log}}}{1.2} \exp \left[ -\frac{1.04(1 + \lambda)}{\lambda - \mu^* - 0.62\lambda\mu^*} \right],
\]

where the Coulomb pseudopotential \( \mu^* \) is set to 0.1, and the electron-phonon coupling constant \( \lambda \) is defined as

\[
\lambda = 2 \int_0^\infty \frac{\alpha^2 F(\omega)}{\omega} d\omega,
\]

and \( \omega_{\text{log}} \) is the logarithmic average frequency,

\[
\omega_{\text{log}} = \exp \left[ \frac{2}{\lambda} \int_0^\infty \log \frac{\omega}{\omega_0} \alpha^2 F(\omega) d\omega \right],
\]

where \( \alpha^2 F(\omega) \) is the Eliashberg spectral function, defined as

\[
\alpha^2 F(\omega) = \frac{1}{2\pi N(E_f)} \sum_q \delta(\omega - \omega_q) \frac{\gamma_q}{\hbar \omega_q},
\]

where \( N(E_f) \) is the density of states (DOS) at the Fermi level and \( \gamma_q \) is the phonon linewidth.

It is very important to include vdW correction methods to describe the interlayer spacing and the out-of-plane lattice constant \( c \) of the quasi-2D layered materials [63]. Due to the lack of a detailed crystal structure of PdSSe, the choice of vdW scheme was based on its sister compounds PdS\(_2\) and PdSe\(_2\) in our previous work [52]. In the present work, further screening was carried out. As shown in Table S1 in the SM [60], without considering the vdW corrections, the standard local-density approximation (LDA) functional excessively underestimates the lattice constant \( c \), while the PBE functional extremely overestimates the lattice constant \( c \). Therefore, the density-dependent energy correction (dDsC) [64,65] was adopted to consider the interlayer vdW interactions. As shown in Table I, the theoretically optimized lattice constants calculated by PBE together with dDsC (hereafter denoted as PBE+dDsC and used for all calculations within VASP, unless otherwise stated) are closer to the experimental value than our previous results (Table I in Ref. [52]), demonstrating the validity of the calculation parameters. Additionally, the energies are comparable with each other for these three polymorphs of PdSSe, and they show a similar structural phase transition and high-pressure superconductivity. Therefore we mainly presented the results and discussions of the AA polymorph of PdSSe in the main text, and the results for the other two polymorphs (AB and BB) were provided in the SM [60].

III. RESULTS AND DISCUSSION

A. Structural evolution under hydrostatic pressure

The structural evolution under compression has been simulated by gradually increasing the pressure from 0 to 10 GPa. As shown in Fig. 2(a), the lattice constants show an anisotropic response to the hydrostatic pressure. Attributed to the weak interlayer connection of vdW bonds, the out-of-plane lattice constant \( c \) significantly shrinks when pressure increases to 3 GPa. In contrast, the lattice constants \( a \) and \( b \) increase slowly. The vdW radii of Pd, S, and Se ions are 2.15, 1.8, and 1.9 Å, whereas the covalent radii of Pd, S, and Se ions are 1.39, 1.05, and 1.20 Å [66,67]. Apparently, the interlayer and intralayer Pd-X bonds belong to vdW and covalent bonds, respectively. Compared with the easily compressed interlayer vdW bonds along the stacking direction, the in-plane intralayer covalent bonds in the (Pd−S\(_2\)−Se\(_2\))\(^{2-}\) square plane are less affected by applied pressure [Fig. 2(b)]. At a pressure of 3.5 GPa, the orthorhombic PdSSe transforms to an intermediate phase. The intermediate phase still has the identical crystallographic symmetry with the ambient-pressure phase, but the out-of-plane lattice constants \( c \) dramatically shrink accompanied by obvious expansions of the in-plane lattice constants \( a \) and \( b \). Meanwhile, the interlayer Pd-X distances between Pd atoms and chalcogen atoms X in the adjacent layer decrease sharply, being close to the intralayer counterparts. This drastic structural change causes a sudden volume collapse [Fig. 2(c)] and energy increase [Fig. 2(d)]. All the lattice constants become equal, and the orthorhombic PdSSe transforms to a cubic phase above 4 GPa (the structure symmetry will discussed later in Sec. II C). Furthermore, three distinct stages of structural transition in the isostructural and isoelectronic PdS\(_2\) and PdSe\(_2\) have been observed by high-pressure experiments, and the 2O orthorhombic phase has been proposed to coexist with the cubic pyrite phase in the intermediate stage [33,34,36]. Regrettably, there are no

| Polymer | \( a (\text{Å}) \) | \( b (\text{Å}) \) | \( c (\text{Å}) \) | \( V_0 (\text{Å}^3) \) | \( E_r (\text{meV/atom}) \) |
|--------|----------------|----------------|----------------|----------------|----------------|
| Expt [11] | 5.595 | 5.713 | 7.672 | 245.23 | – |
| AA | 5.628 | 5.742 | 7.663 | 247.665 | 0.00 |
| AB | 5.631 | 5.740 | 7.664 | 247.718 | 1.60 |
| BB | 5.639 | 5.743 | 7.625 | 246.951 | 1.79 |
experimental studies on PdSSe crystals under pressure to date. Therefore we have to employ the lattice constants at the ambient condition as a starting point and the sister materials PdS\(_2\) and PdSe\(_2\) as references. In addition, we have also checked the structural evolution under pressure with standard PBE and LDA functionals (without considering the vdW corrections). As shown in Fig. S2 in the SM [60], compared to the experimental reported lattice parameters and the transition pressure predicted by PBE+dDsC, LDA underestimates the lattice constant \(c\) and the transition pressure, whereas PBE overestimates the lattice constant \(c\) and the transition pressure. Overall, our theoretical calculations indicate that PdSSe will undergo structural transformation under compression and an intermediate phase may exist during the transition process, which implies that a coexisting region of the orthorhombic phase with the cubic phase may be observed in PdSSe by future high-pressure experiments.

According to the pressure homology principle, the origin of the pressure-induced structural transition of PdSSe from the \(2O\) orthorhombic phase to the cubic phase can be explained by the displacive mechanism [34]. In fact, the layered orthorhombic phase is derived from a structural distortion of the cubic phase, and the unusual (Pd–S\(_2\)–Se\(_2\))\(^{2−}\) square-planar coordination originates from the elongation octahedron along the out-of-plane direction [33,35]. The elongation of the octahedron belongs to the Jahn-Teller (JT) distortion, which is attributed to the degeneracy of the \(d\)-electron state. The JT distortion degree is estimated by a distortive degree parameter \(\Delta_d = 1/6 \sum_{i=1}^{6} [(R_i - \bar{R})/\bar{R}]^2\), where \(R_i\) and \(\bar{R}\) denote individual and average values of the Pd-X bonds, respectively [68]. The out-of-plane chalcogen X ions gradually approach the coordinated central Pd ions with apparent displacements, which leads to a rapid decrease of the distortive degree (\(\Delta_d\)) as a function of pressure below 3 GPa (as shown in Fig. S3 [60]). The interlayer Pd-X distances are about 3.3 (Pd-S).
and 3.2 (Pd-Se) Å at ambient conditions, which are on the verge of the vdW bond (3.1 ∼ 5.0 Å) [35]. The interlayer Pd-X distances shrink quickly along with compression and go below the threshold value of vdW interactions when the pressure increases up to 3 GPa. Further compression leads to the collapse of interlayer spacing and the annihilation of vdW interactions. Consequently, the distortive degree (Δd) of the PdX6 octahedron is sharply suppressed at 3.5 GPa, and the orthorhombic lattice changes to a cubic one when pressure increases up to 4 GPa. Meanwhile, the coordination polyhedron transforms from a square plane into an almost normal octahedron [Figs. 2(e) and 2(f)], as demonstrated by the tiny Δd in Fig. S3 [60]. The electron localization function (ELF) reveals the changes of the interlayer bonding interactions [Fig. 2(g)]. Ranging from 0 to 3 GPa, the ELF is almost zero in the interlayer spacing, where no covalent bond exists. Above 3.5 GPa, the interlayer charge density significantly increases, and a covalent interaction gradually emerges between the metal Pd and the chalcogen X ions in the adjacent layer. The dynamic stability of the cubic phase at 4 GPa is examined by the phonon spectrum. As shown in Fig. S4 [60], the phonon spectrum calculated by the PBE+dDsC and PBE exchange-correlation functional shows evident imaginary frequencies at the Γ point, which can be nearly eliminated by switching to the LDA functional, indicating that such imaginary frequencies are probably not caused by structural instability (a phenomenon which also exists in the monolayer PdSe2 [17]). Therefore the compression almost eliminates the JT distortion in PdSSe and renders the cubic structure stable under high pressure. Recent experiments have shown that PdSe2 underwent a structural transformation from layered orthorhombic phase to cubic pyrite-type structure at 6 ∼ 10 GPa [34,36], while a similar structural transition occurs at a pressure of 16 GPa for its isostuctural compound PdS2 [33]. Our previous theoretical studies have confirmed the emergence of a stable cubic pyrite structure when the JT distortive degree of PdS2 was absolutely eliminated by pressure [35], whereas the distortive degree of cubic-phase PdSSe still retains a certain value due to the different ionic radii of S and Se. Anyway, we can still expect that structural transformations from the layered orthorhombic phase to cubic phase will be realized in PdSSe by high-pressure experiments according to the pressure homology principle [33–36].

B. Electronic structure transitions from semiconductor to semimetal under compression

The pressure-induced structural transition is also accompanied by electronic structure variations. Like many semiconducting TMDC materials [69], as the interlayer distances decrease during compression, the band gaps of PdSSe gradually decrease until complete closure (Fig. S5 [60]). Under ambient pressure, the band structures of all three polyorphs PdSSe show indirect semiconducting characteristics [52]. The calculated band gaps of ∼0.89 eV are slightly larger than the experimental value of 0.65 eV [11], which may be due to the overestimation of the HSE06 functional (Fig. 3). In addition, due to the elongated lattice constants in the c direction, the calculated band gaps in the present paper are slightly larger than those of our previous work (0.62 ∼ 0.78 eV) [52].
This phenomenon indicates that the band gap of PdSSe is extremely sensitive to the interlayer distance, similar to the case of PdSe$_2$ [17]. The band gap of PdSSe closes up at 2.5 GPa. As shown in Fig. 3(a), the band dispersion at 2.5 GPa is very similar to that at 0 GPa, but the valence band maximum (VBM) is higher than the conduction band minimum (CBM), displaying a typical characteristic of semimetal. Further increasing pressure up to 3.5 GPa leads to the lattice transform to an intermediate phase with collapsed interlayer spacing. Though the orthorhombic symmetry remains unchanged, the interlayer interactions are dominant by the covalent bond rather than vdW forces. The collapsed interlayer spacing gives rise to a nearly metallic band structure for the intermediate phase. In fact, there are obvious charge gaps between the valence bands and conduction bands along most parts of the high-symmetric paths [right column of Fig. 3(a)], while they only nearly contact with each other along the high-symmetric paths of Γ-X, Γ-Y, and Γ-Z (see a zoom-in picture of the band structure at 3.5 GPa in Fig. S6 [60]). Therefore the pressure-induced intermediate phase of PdSSe can be still viewed as semimetal.

Previous resistivity experiments observed semiconductor-to-metal transitions in PdS$_2$ (PdSe$_2$) at 7 (3) GPa [33,36]. However, the pressure-induced metallization in PdS$_2$ and PdSe$_2$ occurs before the structural transition to the cubic phase. Therefore the metallization of the intermediate phase in PdS$_2$ and PdSe$_2$ is not related to the cubic structure but originated from the broadening of the energy bands and filling-changes of the Pd-d orbitals around the Fermi level [33,35]. We propose that the pressure-induced metallization in PdSSe can also be explained by an orbital-selective mechanism. As shown in Fig. 3, the distributions of the Pd 4d orbital near Fermi energy are obviously changed under pressure, consistent with the variation of the coordination environments of the Pd atoms. Before the structure changing to the intermediate phase, the $d_{x^2-y^2}$ and $d_z$ orbitals are separated from each other and dominant to the CBM and VBM, respectively [35]. The electronic structural transition from semiconductor to semimetal originates from the bandwidth broadening [middle column of Fig. 3(a)], which can be completely attributed to the increase of the hopping due to the reduced interlayer distance. When the lattice collapses into the intermediate phase, the coordination polyhedron of Pd ion changes from square plane to distorted octahedron. Accordingly, the corresponding energy of the $d_z$ orbital increases, which results in a reduction of the crystal-field splitting between $d_{x^2-y^2}$ and $d_z$ orbitals. Mixed-filled $d_{x^2-y^2}$ and $d_z$ orbitals obviously contribute to the bands around the Fermi level [right column of Fig. 3(a)], implying the orbital-selective mechanism is responsible for the metallization [33,35].

The metallization process can be further inspected by the variation of the band structure combined with local charge density analysis. As shown in Fig. 3(b), we can see obvious variations of the occupied orbital along with the increasing pressure. Similar to PdS$_2$ and PdSe$_2$, the Pd ion has a nominal +2 valence state with 4d$^8$ electron configuration in PdSSe. At ambient-pressure conditions, the 4d electrons of Pd$^{2+}$ preferentially occupy lower energy $d_{xy}$, $d_{xz}$, $d_{yz}$, and $d_z$ orbitals according to the square-planar crystal-field splitting [70]. Therefore the empty $d_{x^2-y^2}$ orbitals locate above the Fermi level and are separated from the occupied $d_z$ orbitals by a charge gap. In addition, the dispersions of the VBM along Γ-X and Γ-Y directions are highly similar at ambient pressure, which are weaker than the highly dispersive bands along Γ-Z direction (left column of Fig. 3), suggesting a strong interlayer coupling interaction [12]. Upon compression, the chalcogen ions X from the adjacent layers get closer to the central Pd atom, resulting in a distorted octahedral coordination. The uppermost valence bands are broadened along with increasing pressure, and the gradually increasing energy of $d_z$ orbital leads to a shrinkage of the energy gap between the $d_{x^2-y^2}$ and $d_z$ orbitals, resulting in a semiconductor-to-semimetal transition (middle column of Fig. 3). Further increasing the pressure, the distortive degree of octahedra is almost annihilated after the collapse of the interlayer spacing (Fig. S3 [60]), and then the interlayer covalent bonds are established. The reductions of crystal-field splitting between $d_{x^2-y^2}$ and $d_z$ orbitals cause a mixture of the empty $d_{x^2-y^2}$ orbitals with the filled $d_z$ orbitals, which forms doubly degenerate $e_g$ states ($d_{x^2-y^2}$ and $d_z$). At 3.5 GPa, the triply degenerate full-filled $t_{2g}$ states ($d_{xy}$, $d_{xz}$, $d_{yz}$) form localized narrow bands at the lower energy region, which are separated from the half-filled $e_g$ states ($d_{x^2-y^2}$ and $d_z$) by a big gap of ~0.57 eV comparable to the counterpart in PdS$_2$ (0.7 eV) [35]. The half-filled $e_g$ states show similar dispersion characteristics along Γ-X, Γ-Y, and Γ-Z directions (Fig. S6 [60]). Especially, the bands crossing the Fermi level along Γ-X and Γ-Y directions are mainly contributed from the $d_{x^2-y^2}$ orbitals, in contrast to the $d_z$ orbitals along the Γ-Z direction, which results in a semimetallic band structure in the intermediate phase (right column of Fig. 3(a) and Fig. S6 [60]). Finally, the intermediate phase transforms into the cubic phase upon pressure increasing to 4 GPa, whose transport properties under high pressure will be discussed in the next section.

C. Topological superconductivity of the high-pressure cubic phase

More interestingly, previous experiments demonstrate that the high-pressure cubic phase PdS$_2$ and PdSe$_2$ show superconductivity and display dome-shaped superconducting diagrams [33,36]. Electron structure analysis of the cubic phase PdS$_2$ and PdSe$_2$ indicates that the superconductivity under high pressure is related to the Dirac states and nodal-line states near the Fermi level [35,36]. As shown in detail in Fig. 4, the band structure of the high-pressure cubic phase PdSSe highly resembles those of the cubic superconducting PdS$_2$ and PdSe$_2$. The bands crossing the Fermi level at the Γ point are considered to be associated with strong electron-phonon coupling and conventional superconductivity. Therefore we speculate that the transport properties of PdSSe are qualitatively similar to the superconductivity of PdS$_2$ and PdSe$_2$ under high pressure.

However, in contrast to the eightfold degeneracies (considering the spin degeneracy) of the energy bands at the M point for the PdS$_2$ and PdSe$_2$, energy bands of PdSSe at
FIG. 4. Comparisons of the band structure of the cubic-phase (a) PdS$_2$, (b) PdSSe (AA polymorph), and (c) PdSe$_2$ at pressure of 4 GPa without (w/o) or with SOC interactions. The green rhombus illustrates the charge gap along the $\Gamma$-R directions. The Dirac and nodal-line states are marked by the red circles in (a) and (c), while they are broken as indicated by the blue circles in (b). The cyan points mark the fourfold and sixfold degenerate fermions at the $\Gamma$ point and R point. The Weyl points along the $\Gamma$-R line are highlighted by the shadow rectangles in (b), which are enlarged as shown in Fig. S8 [60].

the $M$ point split into pairs of fourfold degenerate bands. In addition, the inversion symmetry breaking further lifts the degeneracies of the band structure along the high-symmetric directions when the spin-orbit coupling (SOC) interactions are taken into account. Specifically, the Dirac states and nodal-line states protected by the glide mirror symmetry of the space group $P\bar{a}3$ in PdS$_2$ and PdSe$_2$ are broken in PdSSe. These significant changes of the band structure originate from the absence of inversion and mirror-plane symmetries in PdSSe with respect to those of the cubic pyrite-type PdS$_2$ and PdSe$_2$. Therefore, strictly speaking, the structure symmetry (no. 198 space group $P2_13$) of the high-pressure phase PdSSe (AA polymorph) belongs to the cubic ullmannite-type structure rather than the cubic pyrite-type structure with the no. 205 space group $P\bar{a}3$ [71]. As shown in Fig. 4, the twofold screw rotation ($\tilde{C}_{2f}$) and threefold rotation ($C_3$) symmetries of the nonsymmorphic cubic space groups (no. 198 and no. 205) give rise to exotic fourfold and sixfold degenerate fermions at the $\Gamma$ point and $R$ point, respectively [72,73]. Particularly, the lowest conduction band and the highest valence bands
along high-symmetry lines are completely gapped out after considering the SOC interactions for PdSSe, PdS2, and PdSe2, demonstrating typical characteristics of topological semimetal for these compounds and providing a possible venue for the emergence of nontrivial surface states. We carry out a trial calculation of the symmetry-based indicator and receive a $Z_2 = 1$ for both the cubic pyrite-type PdS2 and PdSe2 (no. 205 space group $Pa3$) [74–77], which indicates strongly topological properties awaiting further detailed investigation. Furthermore, Weyl fermions can arise in the cubic phase PdSSe due to the breaking of inversion symmetry, as demonstrated by the Weyl points along the $\Gamma - R$ line [Fig. 4(b)] induced by the crossing of bands with different C3 eigenvalues [72]. (A close view of the band crossing points near the high-symmetric $R$ point around the Fermi level is presented in Fig. S8 [60].) The superconductivity seems to be intertwined with these topologically nontrivial states [78].

As shown in Fig. S7(b) [60], the Fermi surface of PdSSe consists of a large cubelike pocket at the center of the Brillouin zone and a network of small electron and hole pockets connected along the edges of the Brillouin zone, which are consistent with the multifold degeneracies. The cubelike Fermi surface with small curvature indicates that the cubic-phase PdS2 and PdSSe are likely to produce quantum oscillations with large effective mass [35, 79, 80]. Furthermore, the nontrivial topological states close to the Fermi level contribute considerable DOS values at the Fermi level for the high-pressure phase (Fig. S9) [60], which combined with the large Fermi surface may provide sufficient channels for electron-phonon scattering [81] and favor an enhancement of the electron-phonon interaction [82]. Therefore since the cubic phase PdSSe features similar dispersion characteristics of the band structure, topological states, and Fermi surface with the superconducting phase PdS2 and PdSe2, we expect similar superconducting behaviors will be observed in PdSSe by high-pressure experiments.

In order to confirm the possible superconductivity in cubic-phase PdSSe under high pressure, we calculate the electron-phonon coupling constant $\lambda$ and the superconducting transition temperature $T_c$ for PdSSe. Correspondingly, the phonon DOS (PhDOS) displays three regions separated by two gaps (Fig. 5). The heaviest Pd atoms predominantly contribute to the low-frequency acoustic branches, while the lighter Se atoms contribute to the middle-frequency optical branches. The contributions of the lightest S atoms are very tiny in the low- and middle-frequency region, and predominantly dominate the high-frequency optical branches. The broad distribution of electron-phonon interactions is reflected in the calculated Eliashberg spectral function $\alpha^2 F(\omega)$ [83]. Calculated results show that there are strong electron-phonon interactions in the pressure-induced cubic phase PdSSe. The electron-phonon coupling constant $\lambda$ of the cubic phase PdSSe at 4 GPa is 0.75, and the corresponding superconducting transition temperature $T_c$ is 7.5 K. Therefore the theoretically calculated $T_c$ of cubic-phase PdSSe at 4 GPa is comparable to the theoretical calculated $T_c$ of 4.9 (7.6) K for the cubic pyrite phase PdS2 (PdSe2) at 4 (10) GPa [35]. Furthermore, the experimental observed $T_c$ of the cubic pyrite phase PdS2 and PdSe2 shows dome-shaped dependence on pressure, which increases up to maximum values of 8.0 and 13.1 K at 37.4 and 23 GPa, respectively [33, 36]. We further examine the stability and superconductivity of the cubic-phase PdSSe under pressure. As shown in Fig. S10 [60], the phonon spectra without any imaginary frequencies indicates that the cubic PdSSe can be dynamically stable at 0 GPa. The corresponding PhDOS almost display identical characteristics to that at 4 GPa. The calculated electron-phonon coupling constant $\lambda$ is 0.68 and the corresponding superconducting transition temperature $T_c$ is 5.8 K, which increases along with the increasing pressure. The increasing trend of the theoretically calculated superconducting temperature from 5.8 K (at 0 GPa) to 7.5 K (at 4 GPa) to 10.1 K (at 10 GPa) is in line with the experimental observations [33, 36] and the theoretical calculated results [35] for cubic-phase PdS2 and PdSe2 (Fig. 6). Therefore the pressure-induced evolutions of the crystal structure and electronic transport properties of PdSSe are qualitatively similar to those of PdS2 and PdSe2. The experiments revealed a dome-shaped relationship of the superconducting temperature with the pressure for the high-pressure cubic phase PdS2 (PdSe2), which can increase up to maximum values of 8.0 (13.1) K at 37.4 (23) GPa, respectively. As shown in Fig. 6(b), the $T_c$ of PdSSe is higher than the counterparts of PdS2 and PdSe2 at the studied pressure range, and we can expect it to increase to much higher values by further compression.

Previous experiments indicate that the superconductivity shows a striking correlation with the structural instability of the chalcogen dumbbells in cubic pyrite phase PdSe2 [36]. However, despite showing similar Se-Se bond softening under pressure, the isostructural and isoelectronic pyrite phase NiS2 remains nonsuperconducting up to 50 GPa [33]. Moreover, high-pressure Raman spectroscopy and theoretical calculations do not observe any anomalous softening of the S-S bonding in the isomorphous cubic pyrite phase PdS2 [33, 35]. The symmetric chalcogen Se-Se (S-S) dumbbells in the cubic PdSe2 (PdS2) have been broken and replaced by the S-Se bond in the cubic phase PdSSe. And our theoretical calculations reveal that the S-Se bond lengths in cubic phase PdSSe are nearly independent of pressure (Fig. 2(b)), similar to the rigid S-S bond observed in the cubic pyrite phase PdS2. Therefore the structural instability of the chalcogen dumbbells...
FIG. 6. The evolutions of (a) electron-phonon coupling constants and (b) superconducting critical temperatures of PdS₂, PdSSe, and PdSe₂ along with pressure. The data drawn in green come from our previous theoretically calculated results [35].

is not directly correlated with the emergence of superconductivity in the pyrite-type compounds. The topological nontrivial states around the Fermi level and strong electron-phonon coupling might play a crucial role in triggering the superconductivity in the cubic-phase PdSSe under high pressure. Further experimental studies are needed to clarify.

IV. CONCLUSIONS

In conclusion, we have investigated the transformations of crystal structure and the concomitant evolutions of transport properties in PdSSe under hydrostatic pressure. PdSSe shows a similar structural transition and transport behavior to that observed in its sister compounds of PdS₂ and PdSe₂. Pressure-induced structural transitions from layered orthorhombic phase to cubic phase through an intermediate phase have been theoretically predicted in PdSSe, accompanied by a series of electronic structure transitions from semiconductor to semimetal to superconductor. Electronic structure and electron-phonon coupling calculations indicated that the superconductivity can be realized in the high-pressure cubic phase, which originated from the strong electron-phonon coupling associated with topological nontrivial states. The present study not only reveals the pressure-induced structural transformations and semiconductor-semimetal-superconductor transitions in PdSSe but also provides insights into the metallization and topological superconducting properties of the TMDC compounds under high pressure, which will attract further experimental and theoretical explorations of interesting physics in TMDCs.

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