THE PHYSICAL NATURE OF THE LYMAN-LIMIT SYSTEMS

JASON X. PROCHASKA

Department of Physics and Center for Astrophysics and Space Sciences, University of California, San Diego, C-0424, La Jolla, CA 92093

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ABSTRACT

We analyze Keck HIRES observations of a Lyman-limit system at $z = 2.652$ toward Q2231$-00$. These observations afford the most comprehensive study of the physical properties of a Lyman-limit system to date. By comparing the ionic column densities for Fe$^+$, Fe$^{++}$, Si$^+$, and Si$^{++}$ against calculations derived from the CLOUDY software package, we have strictly constrained the ionization state of this system. This has enabled us to calculate accurate abundances of a Lyman-limit system for the first time at $z > 2$, e.g., [Fe/H] = $-0.5 \pm 0.1$. We also derive a total hydrogen column density of $\log N(\text{H}) = 20.73 \pm 0.2$, which is comparable to values observed for the damped Ly$\alpha$ systems. The system is special for exhibiting C ii$^*$ $\lambda1335$ absorption, allowing us to estimate the electron density, $n_e = 6.5 \pm 1.3 \times 10^{-2}$ cm$^{-3}$. Coupling this measurement with our knowledge of the ionization state, we derive the following physical properties: (1) hydrogen volume density $n_H = 5.9 \pm 1.2 \times 10^{-2}$ cm$^{-3}$, (2) path length $\ell = 3 \pm 1.6$ kpc, and (3) ionizing intensity $\log J_{\text{HI}} = -20.22 \pm 0.21$. We point out that a number of the physical properties (e.g., [Fe/H], $N(\text{H})$, $n_H$) resemble those observed for the damped Ly$\alpha$ systems, which suggests that this system may be the photoionized analog of a damped system. The techniques introduced in this Letter should be applicable to a number of Lyman-limit systems and therefore enable a survey of their chemical abundances and other physical properties.

Subject headings: galaxies: abundances — quasars: absorption lines — quasars: individual (Q2231$-00$)

1. INTRODUCTION

Observations of the quasar absorption line (QAL) systems provide an efficient means for probing the physical conditions of the early universe. Intermediate-resolution surveys have enabled accurate measurements on the evolution of the number density of the QAL systems, including the damped Ly$\alpha$ systems (Wolfe et al. 1986, 1995), the Lyman-limit (LL) systems (Sargent, Steidel & Boksenberg 1989), and the Ly$\alpha$ forest clouds (Sargent et al. 1980). Until recently, the absence of a comprehensive physical description of the various QAL systems has limited the impact of these surveys. With the wealth of data afforded by echelle spectrographs on 10 m class telescopes, one is now capable of making direct measurements of the physical properties of individual QAL systems and, in turn, the role of these systems in galaxy formation and the evolution of the early universe.

Over the past few years, observations of the damped Ly$\alpha$ systems—QAL systems with neutral hydrogen column densities $N(\text{H} \lambda 2) > 2 \times 10^{19}$ cm$^{-2}$—have provided detailed measurements on their chemical composition, ionization state, dust content, metallicity, and kinematic characteristics (Pettini et al. 1994; Prochaska & Wolfe 1996, 1997a; Lu et al. 1996). These observations present vital clues to galaxy formation theory. Thus far, little research has focused on the physical properties of the Lyman-limit systems, QAL systems that are optically thick at the Lyman continuum. Owing to the challenges associated with accurately determining the ionization state of these partially ionized systems, their metallicity and chemical abundances have been poorly constrained. Steidel (1990) performed a survey of the physical properties of $z \approx 3$ LL systems, but the majority of his observations resulted only in limits to the abundances and other properties. With Keck, thus far researchers have focused on the kinematic characteristics of the Mg ii systems (Charlton & Churchill 1996), the majority of which are LL systems. Their efforts have provided keen insight into these systems at moderate redshift $z \approx 1$, but have been somewhat limited by difficulties in identifying their ionization state.

In this Letter, we present techniques aimed at determining the physical characteristics of a single LL system, including measurements of the ionization state, chemical abundances, electron density, and the intensity of ionizing radiation. While the results from this single LL system are not necessarily representative of all LL systems, the techniques outlined in this Letter will be applicable to further LL studies, particularly when $N(\text{H} \lambda 1) > 10^{19}$ cm$^{-2}$. By applying these methods to a significant number of LL systems at high redshift, we will investigate their chemical history, contrast their properties with those of the damped Ly$\alpha$ systems, and thereby probe physical conditions in the early universe. Section 2 presents the observations and measurements of the ionic column densities and the ionization state. In § 3, we determine elemental abundances by making ionization corrections to the ionic column densities. We estimate the electron density, hydrogen volume density, and the intensity of ionizing radiation through an analysis of the fine-structure C ii$^*$ $\lambda1335$ transition. Finally, we provide a brief discussion and summary in § 4.

2. OBSERVATIONS AND ANALYSIS

We observed Q2231$-00$ ($z_{\text{em}} = 3.02$) on the night of 1995 November 1 with HIRES (Vogt 1992) on the 10 m W. M. Keck I Telescope for a total integration time of 2.5 hr. We used the C5 decker plate with 1$''$1 slit, standard 2 $\times$ 1 binning on the 2048 $\times$ 2048 Tektronix CCD, and the kv380 filter. For reduction and calibration of the data, we took a 360 s exposure of the standard star BD +28$^\circ$4211 and images of quartz and Th-Ar arc lamps. The data was reduced and wavelength calibrated with the software package written by T. Barlow and continuum fit with the IRAF package CONTINUUM.

A crucial component in the analysis of any QAL system is

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1 Visiting Astronomer, W. M. Keck Telescope. The Keck Observatory is a joint facility of the University of California and the California Institute of Technology.
the neutral hydrogen column density \( N(\text{H}^+) \). Figure 1 shows the \( \text{H}^\alpha \) line profile for the LL system at \( z = 2.652 \) toward Q2231−00. While the line is heavily saturated, the damping wings are resolved and provide a good measurement of the \( N(\text{H}^+) \) value: \( \log N(\text{H}^+) = 19.12 \pm 0.15 \) dex. The curves in Figure 1 correspond to the line-profile fit (with estimated errors) derived from the VPFIT software package, kindly provided by R. Carswell and J. Webb. We include an estimated 0.15 dex error to the \( N(\text{H}^+) \) value due to the difficulty in determining the unabsorbed continuum flux in the \( \text{Ly}^\alpha \) forest.

Figure 2 presents the velocity profiles of the metal-line transitions observed for this LL system, with \( v = 0 \) corresponding to \( z = 2.652 \). The dotted lines designate regions of the profiles contaminated by other metal lines or \( \text{Ly}^\alpha \) forest clouds. The dashed vertical lines in Fe \( ii \lambda 1608 \) transition indicate the velocity regions discussed below (Table 1). Note that the profiles track one another very closely in velocity space, even across significantly different ionization states (e.g., Fe\( ^+ \), Fe\( ^{2+} \), and Si\( ^{+} \)). As emphasized below, this observation is contrary to that typically observed for the damped \( \text{Ly}^\alpha \) systems (Prochaska & Wolfe 1996; Wolfe & Prochaska 1998). We have measured the ionic column densities from the unsaturated and mildly saturated line profiles by summing the apparent column density \( (N_i(v) = n_i c \ln[I_i(v)/I_{le f}] / \lambda ; \text{Savage & Sembach 1991}) \) over several velocity regions. This approach enables one to calculate ionic column densities as a function of velocity to search for variations in the ionization state, metallicity, and dust depletion. Table 1 lists the column densities for a number of the ions over four velocity regions and the total integrated column densities. We are particularly interested in the relative

![Log N(H) vs Relative Velocity](image1.png)

**Fig. 1.**—\( \text{Ly}^\alpha \) profile of the Lyman-limit system at \( z = 2.652 \) toward Q2231−00. The fit was performed with the VPFIT software package and corresponds to \( \log N(\text{H}^+) = 19.12 \pm 0.15 \) dex, which includes an estimate to the continuum error.

![Velocity Profiles](image2.png)

**Fig. 2.**—Velocity profiles of all the observed metal-line transitions. The dotted regions indicate portions of the profile contaminated by other absorption lines. The dashed vertical lines in Fe \( ii \lambda 1608 \) define the velocity regions discussed in the text.

### Table 1: Ionic Column Densities and Abundances

| Ion    | \( \lambda \) | Reg1 | Reg2 | Reg3 | Reg4 | Total | [X/H] |
|--------|---------------|------|------|------|------|--------|-------|
| H \( i \) | 1215          | ...  | ...  | ...  |      | 19.12  | ±0.2  |
| C \( ii \) | 1334          | 14.24±0.01 | 15.41±0.08 \( a \) | >14.76 | 14.42±0.03 | >15.41 | >−0.85 |
| C \( ii^+ \) | 1335         | ... | 12.90±0.03 | ... | ... | ... | ... |
| O \( i \) | 1302          | 14.49±0.02 | >15.20 | 14.22±0.02 | 13.82±0.02 | >15.33 | >−0.6 |
| Al \( ii \) | 1670          | 12.35±0.01 | >13.80 | 12.88±0.02 | 12.67±0.02 | >13.84 | >−0.75 |
| Si \( ii \) | 1304          | 13.58±0.02 | >14.87 | 14.18±0.01 | 14.03±0.02 | >15.02 | >−0.55 |
| Si \( iv \) | 1402          | ... | >14.50 | >14.21 | >14.09 | >14.78 | ... |
| Fe \( ii \) | 1608          | 12.96±0.08 | 14.34±0.01 | 13.38±0.03 | 13.43±0.03 | 14.44±0.05 | −0.5±0.1 |
| Fe \( iii \) | 1122          | 13.71±0.04 | 14.69±0.03 | 13.86±0.03 | 13.83±0.03 | 14.84±0.02 | ... |
| Ni \( ii \) | 1741          | ... | ... | ... | ... | 13.36±0.04 | −0.78±0.05 |

\( a \) Velocity region spanning \( −100 < v < −20 \) km s\(^{-1}\).
\( b \) Velocity region spanning \( −20 < v < 70 \) km s\(^{-1}\).
\( c \) Velocity region spanning \( 70 < v < 140 \) km s\(^{-1}\).
\( d \) Velocity region spanning \( 140 < v < 210 \) km s\(^{-1}\).

* This value was obtained with the method described in § 3.
To identify the ionization state of this LL system, we have utilized the software package CLOUDY v90.04 (Ferland 1995). Figure 3 presents the predicted ionic column densities versus ionization parameter \( U \) for a model system assuming a Haardt-Madau spectrum (Haardt & Madau 1996), where

\[
U = \frac{\phi_{912}}{\Delta n_{\text{H}}} = \frac{J_{912}}{4\pi h c n_{\text{H}}} = (2 \times 10^{-5}) \frac{J_{912}}{10^{-21.5} n_{\text{H}}/\text{cm}^3}, \tag{1}
\]

where \( n_{\text{H}} \) is the volume density of hydrogen, and \( \phi_{912} \) and \( J_{912} \) are the flux and intensity of the incident radiation at 1 ryd. Note that this is a modified definition of \( U \); it was chosen to facilitate future comparisons with this work. The relative ionic column densities were calculated with the CLOUDY package assuming \( N(\text{H i}) = 10^{12.5} \) cm\(^{-2}\), intrinsic solar abundances, and [Fe/H] = −0.5 dex. The dashed vertical lines denote the range of \( U \) values consistent with the Fe\(^{+}/\text{Fe}^{2+}\) ratio (0.40 ± 0.05 dex), and the dotted line indicates the \( U \) value corresponding to the upper limit on the Si\(^{2+}/\text{Si}^{+}\) ratio (i.e., a lower limit to \( U \)). These observations imply \( \log U = -2.23 ± 0.21 \), which is the most accurate determination of \( U \) in a LL system to date.

3. PHYSICAL PROPERTIES

In the previous section, we presented an accurate measurement of the system’s ionization state by comparing the observed ionic column densities of H\(^{+}\), Fe\(^{+}\), Fe\(^{2+}\), Si\(^{+}\), and Si\(^{2+}\) with the predicted results from a calculation performed with the CLOUDY software package. We find the system is highly ionized with ionization fraction \( x = \text{H}^{+}/\text{H} = 0.97 ± 0.02 \). This implies that the total hydrogen column density \( \log N(\text{H}) = 20.73 ± 0.2 \) is comparable to that observed in the damped Ly\(\alpha\) systems. This value is similar to the estimates from Steidel (1990) for his sample of LL systems. By making the appropriate ionization corrections from the CLOUDY results, we derive the elemental abundances of this system. The logarithmic abundances of element X relative to hydrogen and normalized to solar abundances (Anders & Grevesse 1989), [X/H] = log \( N(\text{X})/N(\text{H}) \) − log \( N(\text{X})_{\odot}/N(\text{H})_{\odot} \), are listed in the last column of Table 1. We find [Fe/H] = −0.5 dex, which is higher than the typical damped Ly\(\alpha\) system and considerably higher than any other estimate to the abundances of a LL system at \( z > 2 \).

To gauge the accuracy with which we have determined the ionization state and thereby the chemical abundances, we have investigated the effects of varying \( N(\text{H}) \) and the shape of the input spectrum. We find that the 0.15 dex uncertainty in the \( N(\text{H}) \) value lends to less than a 0.1 dex uncertainty in [Fe/H] and the majority of other elemental abundances, including the N(\text{H}) value. Furthermore, we considered the effects of a steeper spectrum (e.g., a Bregman-Harrington spectrum; Bregman & Harrington 1986) and find a similar variation in the measured abundances. Examining the relative abundances of this system, we observe little departure from the solar abundance pattern. There is, however, evidence for an overabundance of Si/Fe (the lower limit to [Si/H] is quite conservative given the degree of saturation in the Si profiles) and an underabundance of Ni/Fe as observed in the majority of the damped Ly\(\alpha\) systems. In the damped systems, this pattern is typically interpreted as the result of dust depletion and/or Type II supernovae enrichment. Unfortunately, the S \( \text{ii} \lambda 1253 \) and S \( \text{ii} \lambda 1259 \) profiles in this system are blended with Ly\(\alpha\) forest clouds, since the [S/Fe] measurement is sensitive to both of these interpretations.

The detection of the fine-structure C \( \text{ii} \lambda 1335 \) transition allows further insight into the physical characteristics of this system. The fine-structure line can be excited by several processes, but for a highly ionized system at this redshift, electron collisions dominate (Morris et al. 1986). Therefore, the observed \( N(\text{C} \text{ii} \lambda 1334)/N(\text{C} \text{ii} \lambda 1335) \) ratio provides a measure of the electron density via \( N(\text{C} \text{ii} \lambda 1334)/N(\text{C} \text{ii} \lambda 1335) = 3.9 \times 10^6 n_e \). Unfortunately, the \( N(\text{C} \text{ii} \lambda 1334)/N(\text{C} \text{ii} \lambda 1335) \) ratio cannot be measured directly because the C \( \text{ii} \lambda 1334 \) profile is saturated over the velocity region where the C \( \text{ii} \lambda 1335 \) absorption is detected.

We can accurately estimate the \( N(\text{C} \text{ii} \lambda 1334)/N(\text{C} \text{ii} \lambda 1335) \) ratio, however, provided the assumption that the C \( \text{ii} \lambda 1334 \) and Fe \( \text{ii} \lambda 1608 \) profiles track one another in velocity space. Low ion profiles always track one another in the damped Ly\(\alpha\) systems (e.g., Prochaska & Wolfe 1996; Lu et al. 1996), and one notes that all of the transitions—irrespective of ionization state—track one another in this system. Our approach, then, is to (1) measure \( N(\text{C} \text{ii} \lambda 1334)/N(\text{Fe} \text{ii} \lambda 1608) \) in Reg4, where the effects of saturation are minimal, and (2) correct a \( N(\text{Fe} \text{ii} \lambda 1334)/N(\text{Fe} \text{ii} \lambda 1335) \) measurement in Reg2 by the \( N(\text{C} \text{ii} \lambda 1334)/N(\text{Fe} \text{ii} \lambda 1335) \) ratio estimated in this velocity region. We find \( N(\text{C} \text{ii} \lambda 1334)/N(\text{Fe} \text{ii} \lambda 1335) = 15.41 ± 0.08 \text{ cm}^{-2} \) and correspondingly, \( N(\text{C} \text{ii} \lambda 1335)/N(\text{C} \text{ii} \lambda 1334) = 3.09 ± 0.75 \times 10^{-3} \). Assuming \( n_e/n_\text{H} \approx 1 \) for this highly ionized system, this yields an electron density of \( n_e = 6.5 ± 1.3 \times 10^{-2} \text{ cm}^{-3} \).

The \( n_e \) value coupled with our knowledge of the ionization state enables an estimate of the hydrogen volume density and the intensity of the ionizing radiation. Ignoring the contribution to \( n_e \) from metals (a reasonable assumption when \( x ≈ 1 \)) and

\[ \text{We expect the absorption in Reg4 (} v \approx 170 \text{ km s}^{-1} \text{) for the C } \text{ii} \lambda 1335 \text{ transition is due to an intervening Ly}\alpha \text{ forest cloud and restrict the analysis to the absorption features in Reg2 (} v \approx 20 \text{ km s}^{-1} \text{).} \]
adopting $N(\text{He}^+)/N(\text{He}) = 0.9$ and $N(\text{He}^{++})/N(\text{He}) = 0.1$ from the CLOUDY calculations, we find $n_{H} = 5.9 \pm 1.2 \times 10^{-2} \text{ cm}^{-3}$. With $N(\text{H}) \approx 10^{20.72} \text{ cm}^{-2}$, this implies a path length $\ell \approx N(\text{H})/n_{H} \approx 3 \pm 1.6 \text{ kpc}$. While this length is rather uncertain (greater than 50% statistical error) and does not account for clumping along the sight line, it is still one of the most meaningful size estimates of a QAL system to date. The ionizing intensity $J_{912}$ is easily determined by inverting equation (1): $\log J_{912} = -20.22 \pm 0.21$, which is higher (by a factor of $5 \sim 10$) than typical estimates from the proximity effect (Lu, Wolfe, & Turnshek 1991), but not unreasonably high. Perhaps there is a source of local ionizing radiation (e.g., supernovae, OB stars) in addition to the extragalactic background radiation. Finally, consider the kinematic characteristics of this LL system. First note that the width of the profile spans nearly 200 km s$^{-1}$. Second, we observe that the strongest absorption feature lies at the left edge of the profile and the optical depth decreases monotonically towards positive velocity. This edge-leading asymmetric trait is characteristic of that observed in the damped Ly$\alpha$ systems (Prochaska & Wolfe 1997b, 1998). Contrary to the damped Ly$\alpha$ systems, however, the low ion profiles trace very closely the high ion profiles (Si$^{++}$ and Fe$^{++}$). This indicates that the various ionization stages arise from the same regions within the system. Interestingly, one observes a similar correspondence between the line profiles of multiple ionization stages in the interstellar medium (Savage, Sembach, & Lu 1997). A future survey will determine if a large sample of LL systems exhibits similar traits.

4. SUMMARY AND CONCLUSIONS

We have presented techniques for accurately determining the ionization state of a LL system. The technique requires the measurement of multiple ionization stages of a single element (in this case Fe$^{+}$/Fe$^{++}$), an estimate of $N(\text{H} \,\text{I})$, and a series of calculations with the CLOUDY software package. It should be applicable to a number of high-redshift LL systems and will enable a survey of their elemental abundances. For this system, we find an ionization fraction $x = 0.97 \pm 0.02$ and a corresponding iron abundance [Fe/H] = $-0.5 \pm 0.1$ dex. The overall abundance pattern resembles that observed in the damped Ly$\alpha$ system, possibly suggesting an underlying depletion pattern or Type II supernova enrichment. This system is unusual for exhibiting C II* $\lambda1335$ absorption, which provides one with an estimate of the electron density ($n_{e} = 6.5 \times 10^{2} \text{ cm}^{-3}$). Our knowledge of the ionization state allows estimates of the hydrogen volume density ($n_{H} = 5.9 \times 10^{-2} \text{ cm}^{-3}$), the intensity of the ionizing radiation (log $J_{912} = -20.22$), and the path length through the system ($\ell = 3 \pm 1.6 \text{ kpc}$).

It is instructive to compare this LL system with the properties of the damped Ly$\alpha$ systems. For example, we note that the derived $N(\text{H})$ and $n_{H}$ values are similar to those observed for the damped systems. In fact, if we were not for the high intensity of ionizing radiation, this system would be primarily neutral with $N(\text{H} \,\text{I}) > 2 \times 10^{20} \text{ cm}^{-2}$. The observed abundances and kinematic characteristics further argue for this interpretation. It will be exciting to investigate the connection between other LL systems and the damped Ly$\alpha$ systems through a survey of LL systems at $z > 2$. This research will help develop a better understanding of the connection between the QAL systems and galaxy formation. In addition, a direct comparison with numerical simulations may provide insight into the nature of protogalaxies in the early universe.

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