Graphene on insulating crystalline substrates

S Akcöltekin, M El Kharrazi, B Köhler, A Lorke and M Schleberger

Fachbereich Physik, CeNIDE, Universität Duisburg-Essen, D-47048 Duisburg, Germany

E-mail: marika.schleberger@uni-due.de

Received 16 December 2008, in final form 13 February 2009
Published 25 March 2009
Online at stacks.iop.org/Nano/20/155601

Abstract
We show that it is possible to prepare and identify ultra-thin sheets of graphene on crystalline substrates such as SrTiO$_3$, TiO$_2$, Al$_2$O$_3$ and CaF$_2$ by standard techniques (mechanical exfoliation, optical and atomic force microscopy). On the substrates under consideration we find a similar distribution of single layer, bilayer and few-layer graphene and graphite flakes as with conventional SiO$_2$ substrates. The optical contrast $C$ of a single graphene layer on any of those substrates is determined by calculating the optical properties of a two-dimensional metallic sheet on the surface of a dielectric, which yields values between $C = -1.5\%$ (G/TiO$_2$) and $C = -8.8\%$ (G/CaF$_2$). This contrast is in reasonable agreement with experimental data and is sufficient to make identification by an optical microscope possible. The graphene layers cover the crystalline substrate in a carpet-like mode and the height of single layer graphene on any of the crystalline substrates as determined by atomic force microscopy is $d_{SLG} = 0.34$ nm and thus much smaller than on SiO$_2$.

1. Introduction
Graphene has recently attracted much attention due to its unique electronic properties (see, e.g., [1, 2]). Part of graphene’s attraction comes from the fact that it is fairly easy to produce. The easy preparation of graphene is not only due to the simple mechanical exfoliation process but also in part due to the Si–SiO$_2$ substrate it is usually prepared on, which offers several advantages. It is relatively cheap and easy to obtain, easy to clean, and with an appropriately chosen SiO$_2$ thickness it is very easy to identify even sheets of graphene a single layer thick. As a consequence, the preparation of graphene on SiO$_2$ has been perfected by many groups and a variety of important results have been obtained from this type of sample.

However, there are a number of reasons for studying graphene on a larger variety of substrates. For example, any effects connected to the type of substrate, like doping, binding properties or crystallinity could be studied and possibly exploited. The current focus on SiO$_2$ is not so much given by any unique physical property but simply by the fact that graphene sits on a thin dielectric, which makes it easy to identify even with standard optical microscopy. It was shown that the astonishing visibility of graphene is mainly due to an interference effect between the graphene and the thin layer of SiO$_2$ [3, 4]. The optimum SiO$_2$ thickness to make graphene visible was calculated using the Fresnel formula to be 90 nm. This results in a maximum contrast of $C \approx 12\%$ which is easily visible in a standard optical microscope. In the following we demonstrate that an appreciable contrast can be achieved on bulk dielectrics without the need for thin films. This opens up the possibility of studying graphene on a large variety of substrates, which may be crystalline and have properties and interactions with graphene greatly differing from those of SiO$_2$.

2. Experimental details
We applied the standard exfoliation technique [2] to deposit graphene on SrTiO$_3$(100), TiO$_2$(100), Al$_2$O$_3$(1102) and CaF$_2$(111) single crystal surfaces (Crystec, Korth). These materials are widely used and are commercially available with a very high surface quality. Figure 1 shows atomic force microscope (AFM DI-3100, intermittent contact mode) images of clean samples taken directly from the package without any further surface treatment. Terraces are easily identified, the step edges, however, appear fuzzy, except in the case of CaF$_2$ where straight cleavage steps are typical. The mean roughness
is below 0.5 nm and usually no contamination is detected on the oxidic surfaces, whereas CaF₂ is easily contaminated by adsorbents, most likely water [5]. For optical microscopy (see figure 2) we used an Olympus BX40 (100× NA 0.9), and Raman spectra to determine the number of graphene layers were recorded with a Jobin-Yvon LabRam microscope system. The spectra were excited with a laser of 633 nm wavelength and a laser power of ≈4 mW. Single layer and bilayer flakes were identified via the shape of the 2D line [6].

3. Results and discussion

When sheets of graphene from a single crystal of highly oriented pyrolytic graphite are exfoliated onto a pristine surface of any of those crystals, results as shown in figure 2 are obtained. Typically, flakes the size of several square micrometres stick to the substrate. Most of the flakes are identified as thick sheets of graphite (G), but we also find graphene with a thickness of a few monolayers (FLG) or eventually single layers (SLG). This is comparable with what we find on substrates with 90 nm SiO₂. In the case of CaF₂ adsorbates are trapped underneath the graphene sheet; these influence the contrast and show up as bright patches in the right panel of figure 2(a). The optical contrast compared to graphene on 90 nm SiO₂ is rather poor on all substrates (a few per cent instead of 12%, see table 1) with the exception of CaF₂. But in all cases it is still sufficient to identify regions with single layer flakes.

The clear visibility of even single graphene layers demonstrated in figure 2 is somewhat surprising in view of the general assumption that an appropriately chosen layer of SiO₂ is a prerequisite for good optical contrast. In the following, we will discuss this finding in more detail; this will open up a large class of possible substrates for the investigation of graphene. Abergel et al have already pointed out that in principle a thin film is not necessary to make graphene visible as long as a resonance condition with the substrate is fulfilled [7]. Here, we have made use of another approach to calculate the optical contrast for various substrates.
Figure 2. (a) CaF$_2$, (b) Al$_2$O$_3$, (c) SrTiO$_3$, (d) TiO$_2$. In each panel from left to right: images taken by optical microscopy (left); AFM (middle and right) of graphene crystallites consisting of different numbers of graphene sheets found on the surface region marked by the square. The size of the AFM images is indicated by scale bars.

contrast of a thin layer of graphene on any kind of (semi-infinite) substrate without a thin film in between. It is based on a transfer matrix approach to describe the reflection and transmission properties of an electromagnetic wave interacting with stratified media [8]. For the sake of clarity we assume perpendicular incidence $\theta = 0$. Our system is modelled by a semi-infinite substrate ($z < 0$, index 3), a thin layer of graphene ($0 < z < \Delta$, index 2) and a semi-infinite slab of air ($z > \Delta$, index 1). The transfer matrix associated with the graphene is given by

$$M(\Delta) = \begin{pmatrix} \cos(k_0\hat{n}_2\Delta) & -i\frac{1}{\sqrt{\varepsilon_2}} \sin(k_0\hat{n}_2\Delta) \\ -i\sqrt{\varepsilon_2} \sin(k_0\hat{n}_2\Delta) & \cos(k_0\hat{n}_2\Delta) \end{pmatrix} \tag{1}$$

where $k_0$ is the wavevector and $\hat{n}_2 = \sqrt{\varepsilon_2}$ is the complex refractive index, where the complex dielectric constant is given by the complex electric conductivity, $\hat{\varepsilon} = \frac{\hat{\sigma}}{\varepsilon_0\omega}$. The coefficients
for transmission and reflection are then given by
\begin{equation}
\begin{aligned}
\frac{t}{r} = 
\frac{(m_{11} + m_{12} \hat{n}_1) \hat{n}_1 - (m_{21} + m_{22} \hat{n}_3)}{(m_{11} + m_{12} \hat{n}_1) \hat{n}_1 + (m_{21} + m_{22} \hat{n}_3)} \\
\end{aligned}
\tag{2}
\end{equation}
with \( m_i \) the matrix elements. We are interested in the contrast \( C = \frac{R_c - R_s}{R_s} \) which can be calculated from the reflected intensity with graphene \( R = |r|^2 \) and the intensity of the reflected light without graphene, \( R_0 = \frac{|\hat{n}_1|^2}{|n_1|^2} \). Thus, we need to determine \( r \) by using the matrix elements given by equation (1):
\begin{equation}
\begin{aligned}
\frac{r}{t} = 
\left\{ 
\left( \cos(k_0 \hat{n}_2 \Delta) - \frac{1}{\sqrt{\varepsilon_2}} \sin(k_0 \hat{n}_2 \Delta) \hat{n}_3 \right) \hat{n}_1 \\
- \left( -i \sqrt{\varepsilon_2} \sin(k_0 \hat{n}_2 \Delta) + \cos(k_0 \hat{n}_2 \Delta) \hat{n}_3 \right) \hat{n}_1 \\
\right\}^{-1}
\end{aligned}
\end{equation}

To evaluate this expression we use the fact that the thickness \( \Delta \) of the graphene is orders of magnitude smaller than the wavelength of visible light. Therefore, we treat equation (4) in the limit \( \Delta \to 0 \), and account for the graphene layer using a two-dimensional metallic sheet of conductivity \( \sigma_{2D} \). To calculate the coefficient \( r \) we expand the sine and cosine:
\begin{equation}
\begin{aligned}
\cos(k_0 \hat{n}_2 \Delta) &\approx 1 - \frac{k_0 \hat{n}_2 \Delta}{2}, \\
\sin(k_0 \hat{n}_2 \Delta) &\approx k_0 \hat{n}_2 \Delta - \frac{(k_0 \hat{n}_2 \Delta)^3}{6}.
\end{aligned}
\end{equation}

With these expansions and in the limit of \( \Delta \to 0 \) equation (4) becomes
\begin{equation}
\frac{r}{t} = \frac{\hat{n}_1 - \hat{n}_3 - \frac{\pi}{\varepsilon_2} n_{ge}}{\hat{n}_1 + \hat{n}_3 + \frac{\pi}{\varepsilon_2} n_{ge}},
\tag{5}
\end{equation}

If we take the minimum conductivity of a single layer of graphene \( \sigma_{2D} = \frac{e^2}{\pi \hbar} \) [7] and set \( \hat{n}_1 = 1 \) for air we obtain, for any kind of substrate, \( R = \left( \frac{3.9779 - n_{ge}}{1 + n_{ge}} \right)^2 \). The corresponding contrast values that were obtained for the substrates used in the experiments are listed in table 1. As all imaginary parts here are negligible only the real parts of the refractive indices (taken from [9]) were used for the calculation. For comparison we added the values for graphene on a thin film of SiO\(_2\) as calculated by Blake et al. [4]. The minus sign indicates that the flake will appear brighter than the substrate. The values we find in our experiment are in reasonable agreement with the calculated contrast values. In the case of CaF\(_2\), which yields the highest contrast, the lower experimental value might be due to the adsorbates which are present on CaF\(_2\) cleaved and imaged under ambient conditions [5]. A lower limit for the optical detection of graphene is represented in this study by TiO\(_2\) and SrTiO\(_3\) due to their high refractive index yielding contrast values of only \( C \approx -2\% \).

We analysed the height of single layer (\( d_{SLG} \)) as well as of bilayer graphene (\( d_{BLG} \)) on the different substrates by determining the step height from \( \geq 80 \) individual line scans (see figure 3) for each substrate. The resulting height distributions were fitted by a Gaussian yielding the mean height and the standard deviation. The baseline was determined by averaging over several line scans taken from the respective uncovered substrate. Raman spectra were recorded to provide a definitive identification of single layer and bilayer flakes independently of AFM. In the case of SiO\(_2\), additionally, the interference colours were used to identify single and bilayer flakes. From our combined optical, Raman and AFM data we found an average height of the first graphene layer on SrTiO\(_3\), TiO\(_2\) and Al\(_2\)O\(_3\) of \( d_{SLG} = (0.34 \pm 0.01) \) nm. This is a much lower value than on SiO\(_2\) with \( d_{SLG} = (0.83 \pm 0.02) \) nm (see figure 3), the latter being in good agreement with the literature [10]. The step height between the first and the second layer of graphene is again different on the crystalline substrates compared to SiO\(_2\). For the oxides we found for the thickness of the bilayer \( d_{BLG} = (0.69 \pm 0.02) \) nm, which is twice the value of the single layer. On SiO\(_2\) the value is \( d_{BLG} = (1.2 \pm 0.4) \) nm, yielding an interlayer distance between the first two layers close to 0.4 nm but having a large deviation.

The values on the crystalline substrates of \( d_{SLG} = \frac{1}{2}d_{BLG} = 0.34 \) nm correspond very well to the nominal extension of the unperturbed \( \pi \)-orbitals of a perfect single graphene sheet. This indicates a very high quality of the sheets as well as a strong bonding of the graphene to the crystalline substrate. This is an important finding, as it has already been discussed that the substrate plays a major role in the transport properties of graphene. The substrate induces charged impurities which lead to a locally increased density of charge carriers [11, 12]. A change in mobilities can thus be achieved by controlling the substrate. This is consistent with the experimental observation of high mobilities in free-standing graphene sheets [13].

In an earlier study it was shown that to some extent graphene follows the texture of a GaAs substrate [14]. The authors find that the stiffness of the graphene prevents it from following substrate corrugations greater in height than \( \approx 8 \) nm in accordance with the values found for graphene on SiO\(_2\) [15]. From our AFM images it can be seen that the flakes cover the substrate terraces (corrugation less than 0.4 nm) like a carpet as the step edges are still clearly detected by the AFM, giving the impression of a transparent veil (see figure 4). Note that the steps are reproduced very well but the small-scale variations on the terraces are not (see line scan in figure 4). For graphene sheet thicknesses \( \geq 17 \) ML the step edges can no longer be identified in a topographic image.

4. Conclusions

In conclusion, we have demonstrated that the standard techniques for preparing thin graphene sheets on SiO\(_2\) can be extended to a variety of dielectrics. This opens up an additional range of useful (affordable, easy to handle, high surface quality) substrates and makes it possible to study...
how the interaction of graphene with its supporting material affects its electronic, magnetic and optical properties. From the fact that the measured height of single graphene layers on SrTiO$_3$, TiO$_2$ and Al$_2$O$_3$ is only 0.34 nm, we conclude that this interaction is much stronger for these materials than for SiO$_2$, where the corresponding value is 0.8 nm.

Furthermore, we show experimentally and by transfer matrix calculations that the deposited graphene layers can easily be identified by optical microscopy, which greatly facilitates preparation and inspection. As the exfoliation technique can in principle be extended to ultra-high vacuum conditions (see, e.g., [16]) where preparing clean, atomically
flat, crystalline substrates is a standard procedure, the graphene/substrate interface can be studied under very well controlled conditions. This could be used to study the influence of impurities and defects on the minimal conductivity in graphene [12, 17] in a more systematic way.

Acknowledgments

We gratefully acknowledge financial support from the DFG in the frame of the SFB 616: ‘Energy dissipation at surfaces’. We thank V Buck for granting us access to the Raman spectrometer, M Neubert for his help with the measurements and A Kahlen for providing us with the 90 nm SiO2/Si substrate.

References

[1] Novoselov K S, Jiang D, Schedin F, Booth T J, Khotkevich V V, Morozov S V and Geim A K 2005 Proc. Natl Acad. Sci. 102 10451
[2] Geim A and Novoselov K S 2007 Nat. Mater. 6 183
[3] Ni Z H, Wang H M, Kasim J, Fan H M, Yu T, Wu Y H, Feng Y P and Shen Z X 2007 Nano Lett. 7 2758
[4] Blake P, Hill E W, Castro Neto A H, Novoselov K S, Jiang D, Yang R, Booth T J and Geim A K 2007 Appl. Phys. Lett. 91 063124
[5] Akcöltekin S, Roll T, Akcöltekin E, Klusmann M, Lebius H and Schleberger M 2009 Nucl. Instrum. Methods B 267 683
[6] Ferrari A C et al 2006 Phys. Rev. Lett. 97 187401
[7] Abergel D S L, Russell A and Fal’ko V I 2007 Appl. Phys. Lett. 91 063125
[8] Born M and Wolf E 1983 Principles of Optics 6th edn (Oxford: Pergamon)
[9] Lide D R (ed) 1957 CRC Handbook of Chemistry and Physics 87th edn (London: Taylor and Francis)
[10] Obraztsova E A, Osadchy A V, Obraztsova E D, Lefrant S and Yaminsky I V 2008 Phys. Status Solidi b 245 2055
[11] Adam S, Hwang E H, Galitski V M and Sarma S D 2007 Proc. Natl Acad. Sci. 104 18392
[12] Chen J H, Jang C, Adam S, Fuhrer M S, Williams E D and Ishigami M 2008 Nat. Phys. 4 377
[13] Du X, Skachako I, Barker A and Andrei E Y 2008 Nat. Nanotechnol. 3 491
[14] Stöberl U, Wurstbauer U, Wegscheider W, Weiss D and Eroms J 2008 Appl. Phys. Lett. 93 051906
[15] Ishigami M, Chen J H, Cullen W G and Fuhrer M S 2008 Nano Lett. 7 1643
[16] Ritter K A and Lyding J W 2008 Nanotechnology 19 015704
[17] Tan Y-W, Zhang Y, Bolotin K, Zhao Y, Adam S, Hwang E H, Das Sarma S, Stormer H L and Kim P 2007 Phys. Rev. Lett. 99 246803