The transition from school to university in mathematics education research: new trends and ideas from a systematic literature review

Pietro Di Martino1 · Francesca Gregorio2,3 · Paola Iannone4

Accepted: 3 October 2022 / Published online: 11 November 2022 © The Author(s) 2022

Abstract
Investigating the transition between educational levels is one of the main themes for the future of mathematics education. In particular, the transition from secondary school to STEM degrees is problematic for the widespread students’ difficulties and significant for the implications that it has on students’ futures. Knowing and understanding the past is key to imagine the future of a research field. For this reason, this paper reports a systematic review of the literature on the secondary-tertiary transition in Mathematics Education from 2008 to 2021. We constructed two corpuses: one from the proceedings of three international conferences in mathematics education (PME, ICME, and INDRUM) and the other from peer reviewed research papers and book chapters returned by the databases ERIC and Google Scholar. A clear evolution in perspectives since 2008 emerges from the analysis of the two corpuses: the research focus changed from a purely cognitive to a more holistic one, including socio-cultural and — to a lesser extent — affective issues. To this end, a variety of research methods were used, and specific theoretical models were developed in the considered papers. The analysis also highlights a worrisome trend of underrepresentation: very little research comes from large geographical areas such as South America or Africa. We argue that this gap in representation is problematic as research on secondary tertiary transition concerns also consideration of socio-cultural and contextual factors.

Keywords Secondary-tertiary transition · Systematic literature review · Epistemological affective and socio-cultural approaches · Undergraduate mathematics students · Rite of passage

1 Introduction

The study of the transition from secondary school to university mathematics — also referred to as the secondary-tertiary transition (STT) — has a long tradition in mathematics education research. Seminal studies were conducted by Tall since the 1980s, investigating significant cognitive discontinuities in STT (Tall, 1991; Tall & Vinner,
Tall’s studies inspired the development of research specifically focused on students’ difficulties in STT. At the end of the past millennium, De Guzman et al. (1998) summarised the main findings of this field of research and identified three categories related to students’ difficulties in STT: epistemological-cognitive, sociological-cultural, and didactical.

A quarter of a century later, students’ difficulties in STT are still a significant issue for modern society. The high dropout of undergraduate students in STEM subjects reported in several countries (Rach & Heinze, 2017) is problematic for at least two reasons. The first relates to the need of advanced mathematics competencies for economies to flourish (Adkins & Noyes, 2016). The second is linked to equity, given the opportunities afforded by STEM degrees (science, technology, engineering, and mathematics) in terms of social mobility and future earnings (see Higher Education Statistics Agency, 2018, for the UK context). Indeed, the European Mathematical Society recently conducted a survey amongst mathematicians to collect information to devise national and international actions that may help reduce students’ dropout during the STT (Koichu & Pinto, 2019). The authors underline that the STT is a complex and multi-faceted process, provoking frustration in first-year students, as well as in lecturers.

The difficulties that students encounter when moving from school mathematics to the mathematics in a STEM degree still represent a strange story, not fully explained, that involves and overwhelms even students considered excellent in mathematics during their school experience (Di Martino & Gregorio, 2019). Understanding this complex and apparently unexplained phenomenon requires many theoretical approaches and, as Schoenfeld (2000) notices, ‘findings are rarely definitive; they are usually suggestive. Evidence is not on the order of proof but is cumulative’ (p. 648). This cumulative nature of findings suggests the relevance of literature reviews on selected topics: they allow researchers to identify trends and provide insights for possible developments of the research field (Pan, 2016).

An influential review of research on STT was conducted by Gueudet in 2008. Gueudet highlights three types of transitions involving individual, social, and institutional factors: transition in ways of thinking, transition to proof and the technical language of mathematics, and institutional transition related to changes in the didactical contract. Gueudet’s review also confirms that up to that time, the tertiary transition in mathematics was mainly studied through cognitive and epistemological lenses, even though socio-cultural and affective issues had since assumed an important role in mathematics education (Lerman, 2000). Gueudet (2008) concludes that there is ‘the need for further research, and for teaching designs grounded in their findings’ (p. 252). Her call was heard by the mathematics education research community, and research on STT has since adopted new theoretical perspectives, discussed new results, and highlighted new lines of interest. Indeed, the transitions to higher education are one of the themes emerging from a recent international survey of researchers in mathematics education answering the question: ‘on what themes should research in mathematics education focus in the coming decade?’ (Bakker et al., 2021, p. 2).

Recently, Bergsten and Jablonka (2019) traced the development of studies on STT in terms of the theoretical approaches taken. However, a systematic review of the research on STT in the last 15 years is still missing. To fill this gap, we analyse the research on STT in mathematics education since 2008.

We developed our systematic review to answer the following research questions related to the period 2008–2021:

RQ1: Which are the methods and the specific theoretical frameworks used to approach STT?
RQ2: What are the main themes of STT research emerging from an analysis of published research?

RQ3: What is the geographical distribution of STT research? Do we know enough about diverse cultural context coming from a wide range of countries?

2 Methodology

The development of a systematic review involves several aspects: in this section, we briefly describe the underlying choices of our review and their reasons, as well as its constraints and the possibility of reproducibility.

The development of a literature review is a systematic process (Pan, 2016), involving three steps needed to identify the corpus of interest (Green et al., 2006): selection of the topic, definition of the sources of information, and definition of the selection criteria employed (Table 1).

The relevance of the topic and the reasons for the review (Step 1) were discussed in the introduction of this paper.

The description of Steps 2 and 3 is of crucial importance for a systematic literature review: it allows other scholars to replicate the selection of the corpus by following the given criteria. Related to these two steps, we differentiate between the two searches we conducted: one focused on conference proceedings, the other on refereed journal papers and book chapters. For both searches, the starting year was 2008 and the ending was October 2021. However, the database and, in part, the automatic search criteria were different between the two searches.

According to our focus, we included in this review studies describing the STT to university mathematics of students enrolled in STEM degrees. These studies may involve pre-service secondary mathematics teachers in those countries where they are taught mathematics in the same lectures of students enrolled in a STEM degree. However, we consider the STT for pre-service teachers (including teachers for primary and lower secondary education) as a special case of transition to tertiary mathematics deserving, in our view, a separate discussion, not addressed in this paper.

We developed a specific search for conference proceedings since international conferences are likely to be a forum to share ideas which are then developed in journal papers or book chapters, and results emerging from conference proceedings often anticipate trends in the development of research themes.

The first choice we made was related to which conference’s proceedings to include in the review. We decided to include two of the most popular (by number of participants) international conferences in mathematics education: the International Congress on Mathematical Education (ICME) and the Conference of the International Group for

| Step 1: Selection of the topic | Step 2: Sources of information | Step 3: Selection criteria |
|-------------------------------|-------------------------------|----------------------------|
| Why the topic is relevant?    | Database                      | Automatic search criteria  |
| Why a literature review about the topic is needed? | Starting and ending year of the search | Selection criteria used to include or exclude in the review a study selected by the automatic criteria |
the Psychology of Mathematics Education (PME). For the likely relevance to our focus, we also included the conferences organised by the International Network for Didactic Research in University Mathematics (INDRUM).

Since our third research question concerned the representation of geographical regions in mathematics education research, one of the main reasons for the selection of ICME, PME, and INDRUM was that the international program committees of these conferences are open to members coming from all over the world. Using this criterion, we did not include in our search other potentially relevant conferences such as CERME (Congress of the European Society for Research in Mathematics Education), RUME (the Research on Undergraduate Mathematics Education of the Mathematical Association of America), PME-NA (North American Chapter of the International Group for the Psychology of Mathematics Education), and other PME regional conferences.

The database for the construction of this first corpus therefore consisted of the published proceedings of ICME, PME, and INDRUM since 2008. We identified all the contributions including the key term ‘transition’ in the title, abstract, or text (automatic search criterion). We then considered only contributions where the occurrence was related to the secondary-tertiary transition and with STT as the significant focus of the paper (not mentioned as a secondary topic).

For the construction of the second corpus (which includes journal papers and book chapters), we first considered what search criteria to use, as this is a crucial step for every literature review. Gusenbauer and Haddaway (2020) recognised three main quality criteria for literature searches: completeness (identifying all the most significant resources about the topic), transparency, and reproducibility. Through the analysis of the systematic search qualities of 28 academic search engines, the authors suggested to conduct literature reviews using at least two different search engines, according to their quality with respect to the three criteria mentioned above. Regarding Google Scholar, Gusenbauer and Haddaway (2020) observe that this search engine has several limitations in terms of transparency and reproducibility of searches; however, ‘it is considered a suitable supplementary source of evidence (including on grey literature)’ (p. 196) for systematic literature reviews.

Based on the above considerations, we used two databases: ERIC (Education Resources Information Center, https://eric.ed.gov), the online database of education research promoted by the US Department of Education, and Google Scholar (https://scholar.google.com). The use of Google Scholar in our review appeared important to bring to the fore contributions by researchers who may not have access to the main journals and conferences of our community (for example due to the high cost of conference fees and travel). We also followed Haddaway et al.’s (2015) advice to focus on the first 200 to 300 results returned by Google Scholar for systematic reviews as supplementary source of evidence.

Since the databases were not specific to mathematics education, we used a strict automatic search criterion. We used ‘transition AND mathematics AND school AND university’ as search terms. We observed a posteriori that the inclusion of the word ‘university’ in the Google Scholar search was not useful: Google Scholar searches the entire document — unlike ERIC which searches only the title, the abstract, and the keywords — and therefore the word university featured in all documents where the names of authors and their institutions were included. At the end of this first phase, following the recommendation of Haddaway et al. (2015), we considered the corpus produced by the union of the 252 results produced from ERIC and the first 300 results by relevance from Google Scholar taking care to eliminate repetition of entries between the two sets of results since, as expected, there was a significant overlap.
The selection criteria used to include a study identified using the automatic search criteria were the same for both databases. Assuming the definition of STT given in the Encyclopaedia of Mathematics Education as ‘the process experienced by students leaving secondary school and entering different kinds of postsecondary institutions: universities, engineering schools, etc.’ (Gueudet & Thomas, 2020, p. 762), we selected the contributions describing a transitional process, considering a ‘before’ and an ‘after’ this process. This means we excluded studies where the focus was solely on one of the stages of this transition (e.g., students’ experiences with proof at the start of a mathematics degree) and did not consider the ‘before’ and ‘after’ of the STT. Because of this choice, papers focusing on the design of transition to proof courses or university preparatory classes were not included in our review.

A margin of subjectivity in the application of the selection criteria clearly exists in this process. However, the first two authors developed an investigator triangulation to balance individual biases (Mok & Clarke, 2015). The two authors applied independently the selection criteria, sharing their outcome. They then discussed the cases of disagreement until a full agreement for the selection of the final corpuses was reached.

The result of this process was the two final corpuses: the first one including 59 reports presented in the three selected conferences and the second one including 55 papers from peer reviewed journals and books.

Once we selected the corpus, aligned with the research questions of the systematic review, each paper was categorised according to: year of publication, type of study (theoretical, empirical, didactical design) and — if empirical — methods (quantitative, qualitative, mixed), instruments, sample, context1 (country where the research was developed, how many and which schools, university, or texts were involved in the research), theoretical framework(s), research question(s), and focus (cognitive, affective, socio-cultural). This classification allowed for multiple labels: for example, a paper could be classified with cognitive and socio-cultural foci if explicit references to both cognitive and socio-cultural issues were made in the theoretical framework or in the research question(s).

In addition to the described classification, we also noted the main findings of the study for each paper.

The recognition of the main research themes was based on a coding process related to the research questions aimed to recognise frequencies and patterns (Cohen et al., 2007). Initially, a very specific label was assigned to each research question of the paper considered, then — following Miles et al. (2003) — the labels evolved during the process to describe wider categories capable to bring together several similar focuses (an example of this evolution is summarised in Fig. 1).

---

1 For the theoretical studies, we reported and considered the author’s nationality.
3 Results and discussion

3.1 STT in conference proceedings from 2008 to 2021

As previously described, we considered in our review three international conferences: ICME, INDRUM, and PME.

3.1.1 ICME congresses

ICME is a large international congress held every 4 years involving researchers worldwide. Four ICME congresses took place since 2008: the proceedings of ICME-11 (Monterrey, Mexico 2008) and of ICME-14 (Shanghai, China, 2021, online conference) are not currently available, while those of ICME-12 (Seoul, Korea, 2012) and ICME-13 (Hamburg, Germany, 2016) are published as open access Springer books. According to the spirit and nature of the activities of the Topic Study Groups (TSG), the existing proceedings consist of abstracts of the discussions developed in the sessions rather than a collection of research reports. For this reason, the discussion which follows is short and mainly descriptive.

The evolution of the presence of STT in the discussion of the ICME community can be recognised by the analysis of the proceedings, scientific programs, and books related to developed activities. In what follows, we detail the evolution of research on STT within these four ICME congresses.

Although one of the TSGs of ICME-11 was about university mathematics, STT was not mentioned in the description of its scientific program.

The situation was different 4 years later at ICME-12. The transition ‘problem’ was explicitly mentioned in the call for papers and in the description of TSG 2: ‘Mathematics education at the tertiary level and access to tertiary level’. Within this TSG, we found five contributions on STT by authors from five different continents (Brazil, Canada, South Korea, South Africa, Sweden). Four out of these five contributions analysed students’ difficulties with specific mathematics topic (matrices, axiomatic method, calculus) with a predominantly cognitive approach. There was also a survey team dedicated to STT, and the outcomes of this work were findings of an international survey of 79 mathematics lecturers from 21 countries. Findings pointed to ‘a multi-faceted web of cognitive, curricular and pedagogical issues’ (Thomas et al., 2015, p. 278) related to STT, also depending on the institutional context. Despite the evident differences between institutions, and therefore the emergence of socio-cultural aspects, the lens of this survey is still strongly cognitive, without specific reference to affective issue. However, the final mention of the emerging interest for how students experience their first encounters with advanced mathematical topics represented a first step towards the inclusion of affective issues in the discussion.

At ICME-13, STT was a recurrent topic: seven contributions presented in TSG2: ‘Mathematics education at the tertiary level’ were focused on STT. In addition, transition issues were the topic of a discussion group and of the plenary panel. The latter inspired an ICME monograph where the main results of the research and ‘the blind spots that remain unquestioned’ (Gueudet et al., 2016, p. 19) were discussed. The summary of the results included considerations about institutional differences (for example in class size or equipment) and pedagogical and cognitive issues, but no mention of affect was made.

At ICME-14, four contributions in TSG2 were focused on STT. In particular, Pinto, Gamlieli, and Koichu discussed the results of an international survey conducted among
310 tertiary mathematics lecturers from 30 countries. This confirms the potential of ICME Congresses to foster discussion between researchers from different contexts. The wide geographical reach of the ICME Congresses is particularly relevant for research on STT considering that international comparisons are still rare elsewhere in our field.

To conclude, the diachronic analysis of the proceedings and scientific programmes of these four ICME editions shows an increasing interest for STT. However, while a lack of attention to affective issues clearly emerges, the discussion about socio-cultural issues is promoted through the involvement of researchers from a variety of countries, with a considerable participation of researchers from countries currently underrepresented in mathematics education.

3.1.2 INDRUM conferences

The growing interest for undergraduate mathematics education in our field is also evidenced by the foundation of the International Network for Didactic Research in University Mathematics (INDRUM) in 2015. Since 2016, this network holds a biannual conference with open access to online proceedings. To date, the following conferences have been held: INDRUM 2016 (Montpellier, France, Nardi et al., 2016), INDRUM 2018 (Kristiansand, Norway, Durand-Guerrier et al., 2018), and INDRUM 2020 (virtually held in Bizerte, Tunisia, Hausberger et al., 2020). The book Research and Development in University Mathematics Education (Durand-Guerrier et al., 2021) provides a detailed overview of the discussion on topics in the 2016 and 2018 INDRUM conferences. Focusing on STT and according to our criteria, we identified 18 contributions relevant to our review (Table 2).

We first notice a clear prevalence (78%) of contributions by European researchers, probably related to the origin of the INDRUM group. Within this European prevalence, there is a strong presence of French authors who account for 39% of the reports on STT. The French influence on the INDRUM community is not only evident in terms of participation: it is also evident from the theoretical frameworks used in the research reports included in the proceedings of these conferences.

Three out of the four theoretical papers on STT used the anthropological theory of the didactic (ADT) (Chevallard, 1992) for identifying praxeologies in STT. The fourth, the paper by Artigue (2016), discussed the challenges of the research in mathematics education at the tertiary level. As for the empirical papers, four reported and interpreted students’ difficulties in STT using the lens of the anthropological theory of didactic. The common hypothesis of these studies was that several phenomena in STT can be interpreted as institutional issues, determined by the strong discontinuity between school and university praxeologies. This approach was extensively described in Gueudet and Pepin (2017).

Using this framework, Winsløw (2008) introduced a model with repeated cycles of two transitions to university mathematical praxeologies: the first is related to the need for students to extend their praxeologies considering the role of theory in mathematics. The second transition takes place when the elements of the theory become objects; students need to work with autonomously: in this case, the emergence of new objects can require further transitions.

Other important theoretical frameworks developed by French researchers and adopted in papers included in the INDRUM proceedings for studying STT are the theory of didactical situations (Brousseau, 2002) — that Bloch and Gibel (2016) used for developing a tool for modelling students’ reasoning processes — and the Instrumental Approach (Rabardel, 2002), used by Gueudet and Pepin (2016) for theorising the use of technology in STT.
| Author(s)                     | Type of study | Method   | Sample and instruments                                                                 | Context                        |
|------------------------------|---------------|----------|----------------------------------------------------------------------------------------|--------------------------------|
| Artigue (2016)               | Theoretical   | –        | –                                                                                      | France                         |
| Bloch and Gibel (2016)       | Empirical     | Qualitative | 14 university students (students’ scripts from the final exam)                        | France                         |
| Gueudet and Pepin (2016)     | Empirical     | Qualitative | 86 university students, 1 university teacher (interview, online questionnaire, students’ scripts) | France and UK                  |
| Hausberger (2016)            | Theoretical   | –        | –                                                                                      | France                         |
| Nihoul (2016)                | Empirical     | Qualitative | 24 university students (students’ scripts)                                              | Belgium                        |
| Petropoulou et al. (2016)    | Empirical     | Qualitative | 1 lecturer (direct observation of lessons, interview)                                  | Greece                         |
| Quéré (2016)                 | Empirical     | Qualitative | 179 university students (online questionnaire)                                         | France                         |
| Vandebruck and Leidwanger (2016) | Empirical     | Mixed     | 513 university students (online questionnaire)                                         | France                         |
| Brandes and Hardy (2018)     | Theoretical   | –        | –                                                                                      | Canada                         |
| Broley and Hardy (2018)      | Empirical     | Qualitative | Analysis of lecturers’ assignments and exams                                            | Canada                         |
| Geisler and Rolka (2018a)    | Empirical     | Quantitative | 193 university students (questionnaire)                                                | Germany                        |
| Gradwohl and Eichler (2018) | Empirical     | Quantitative | 182 university students (questionnaire)                                                | Germany                        |
| Hochmuth (2018)              | Theoretical   | –        | –                                                                                      | Germany                        |
| Kock and Pepin (2018)        | Empirical     | Qualitative | 24 university students, 2 lecturers, 1 tutor (interview)                              | The Netherland                 |
| Rach et al. (2018)           | Empirical     | Quantitative | 339 university students (questionnaire, students’ script)                              | Germany                        |
| Doukhan (2020)               | Empirical     | Quantitative | 29 secondary students, 25 university students (students’ scripts)                      | France                         |
| Flores Gonzalez et al. (2020) | Empirical     | Qualitative | 1 lecturer (Analysis of course reference books, interview)                            | Brazil                         |
| Khalloufi-Mouha (2020)       | Empirical     | Qualitative | 1 lecturer (Analysis of two schoolbooks and lecturer’s notes)                        | Tunisia                         |
The INDRUM papers pay great attention to cognitive and epistemological issues in STT; several of the authors’ theoretical approaches fall under the umbrella term advanced mathematical thinking’ (Hochmuth et al., 2021, p. 195) and are often situated within APOS (action-process-object-schema) theory (Dubinsky, 1991). However, the use of the ATD also shows some consideration of institutional and social perspectives, but only one paper (Gueudet & Pepin, 2016) analysed and compared two case studies from different national contexts (France and UK).

Only two papers in our INDRUM sample have an affective focus. Quéré (2016) analysed the different forms of autonomy required in the move from secondary to tertiary education in mathematics, also discussing the role of theories of success and expectations in students’ difficulties in STT. Geisler and Rolka (2018b) discussed the relationship between students’ success in mathematics in their first university year and some affective variables (self-concept, interest, view of mathematics, basic needs, self-efficacy).

3.1.3 PME conferences

PME conferences have annual frequency; therefore, we analysed 13 editions: from Mexico 2008 to the edition virtually held in Thailand in 2021. PME includes several types of contributions and activities: research report, short oral, working group, discussion group, poster, and plenary. In the following, we will focus on the 26 selected research reports (Table 3).

Table 3 illustrates both a small but steadily growing presence of empirical research reports on STT since 2009, and the absence of theoretical reports. The latter may also result from the strict length limitation of the contributions. The analysis of representation by country returns a clear picture: 23 out of 26 reports (88%) were developed in a European country by European researchers (one of these papers discusses a comparison between France and Brazil, also involving a Brazilian author). These data highlight an issue of underrepresentation in the PME conferences concerning the discussion about STT.

Moreover, 16 (62%) out of 26 reports are by researchers from German universities. This regional predominance is also reflected in the research methodologies: the quantitative approach is prevalent in these empirical studies (62.5% versus 29% for the qualitative approach and 8% for the mixed one), and samples are usually large, notwithstanding the presence of three interesting case studies. Several reports focus on the identification of significant correlations between academic success/failure and other variables. This aim is related to a clear definition of the variables involved, to the development of instruments for measuring these variables and the students’ success or failure, and to the adoption of statistical models (the more frequently adopted being the Rasch model).

Considering the 7-year period 2008–2014, we found 9 research reports about STT measuring students’ preparedness in mathematics and students’ learning strategies at the beginning of their university experience. These studies aim to determine whether and to what extent mathematics dropout can be predicted by the analysis of cognitive performance at the beginning of university (Halverscheid & Pustelnik, 2013). In first period, two exceptions are represented by the paper by Di Martino and Maracci (2009), stressing the need to go beyond a purely cognitive approach also in research about STT, and the paper by Dias et al. (2010), that, within the ATD framework, developed a socio-cultural comparison...
| Author(s)                        | Type of study | Method                  | Sample and instruments                                                                 | Context       |
|---------------------------------|---------------|-------------------------|----------------------------------------------------------------------------------------|---------------|
| Duhl (2009)                     | Empirical     | Qualitative             | Analysis of official curricula                                                            | Denmark       |
| Di Martino and Maracci (2009)   | Didactical Design | –                      | –                                                                                      | Italy         |
| Klymchuk and Thomas (2009)      | Empirical     | Qualitative             | 178 school and university teachers (questionnaire)                                       | New Zealand   |
| Dias et al. (2010)              | Empirical     | Qualitative             | Analysis of official curricula and tasks used for the entrance selection                 | Brazil, France|
| Rach and Heinzle (2011)         | Empirical     | Quantitative            | 118 university students (questionnaire, final school grades)                             | Germany       |
| Halverscheid and Pustelnik (2013)| Empirical    | Quantitative            | 294 university students (exam results)                                                   | Germany       |
| Hong and Thomas (2013)          | Didactical Design | –                      | –                                                                                      | Korea, New Zealand |
| Schäfer (2013)                  | Empirical     | Qualitative             | 2 pairs of students (interview)                                                          | Germany       |
| Beitlich et al. (2014)          | Empirical     | Quantitative            | 6 lecturers and 2 two university students (eye tracking)                                 | Germany       |
| Halverscheid et al. (2015)      | Empirical     | Quantitative            | 1134 university students (test results)                                                  | Germany       |
| Ufer (2015)                     | Empirical     | Quantitative            | 333 university students (students' scripts from a text, final school grades, self-report about study motives) | Germany       |
| Jeschke et al. (2016)           | Empirical     | Quantitative            | 661 university students (questionnaire, measures of self-concept and interest in mathematics) | Germany       |
| Ottinger et al. (2016)          | Empirical     | Quantitative            | 159 university students (students' scripts)                                              | Germany       |
| Pustelnik and Halverscheid (2016)| Empirical   | Quantitative            | 584 university students (test results, degree course, time gap, and duration of school attendance) | Germany       |
| Griese (2017)                   | Empirical     | Quantitative            | 255 university students (questionnaire)                                                  | Germany       |
| Kouvela et al. (2017)           | Empirical     | Qualitative             | 2 students (interview, focus group)                                                      | UK            |
| Pigge et al. (2017)             | Empirical     | Quantitative            | 36 university teachers (online questionnaire)                                            | Germany       |
| Bampili et al. (2018)           | Empirical     | Qualitative             | 2 university students (interview)                                                        | Greece        |
| Di Martino and Gregorio (2018)  | Empirical     | Qualitative             | 127 university students (questionnaire, interview)                                       | Italy         |
| Geisler and Rolka (2018b)       | Empirical     | Quantitative            | 155 university students (2 questionnaires)                                              | Germany       |
| Maciejewski (2018)              | Empirical     | Mixed                   | 116 university students (short answers to an open prompt)                                | USA           |
| Meehan et al. (2018)            | Empirical     | Quantitative            | 33 university students (questionnaire)                                                   | Ireland       |
| Geisler and Rach (2019)         | Empirical     | Quantitative            | 89 mathematics freshmen (2 questionnaires)                                              | Germany       |
| Roos (2019)                     | Empirical     | Mixed                   | 89 university students (questionnaire)                                                   | Germany       |
| Geisler (2021)                  | Empirical     | Quantitative            | 222 university students (two questionnaire)                                             | Germany       |
| Rach (2021)                     | Empirical     | Quantitative            | 150 university students (questionnaire)                                                  | Germany       |
between Brazil and France regarding STT, considering differences in educational systems and in educational cultures.

In the subsequent 7-year period (2015–2021), we found 17 research reports about STT. The clear difference in the number of reports between the period 2008–2014 and the period 2015–2021 highlights the growing interest for STT in the mathematics education community. The analysis of the frameworks and the research questions used in the research reports in the period 2015–2021 shows a greater consideration for affective and socio-cultural constructs in STT research. Ufer (2015) analysed the relationship between students’ motivations to choose a mathematical programme and their success, Jeschke et al. (2016) attempted to measure students’ ‘academic buoyancy’ and its role in early dropout, and Kouvela et al. (2017) studied the students’ identities as mathematics learners and the influence that messages given by their lecturers have on the development of these identities.

The 2018 edition of PME in Umeå deserves special attention because of its variety of approaches to STT. Bampili et al. (2018) analysed how social and institutional issues shape the development of a new identity for first year mathematics students by adopting the theoretical framework of Communities of Practice (Wenger, 1998). Meehan et al. (2018) studied how STT affects high-achieving students’ ‘sense of belonging to math’, that is related ‘to whether one feels a member of a mathematical community and feels valued and accepted by that community’ (p. 371). Di Martino and Gregorio (2018) introduced and analysed the so called ‘first-time phenomenon’, that is the cognitive and emotional reactions of (successful) students to the first experience of failure in mathematics. Geisler and Rolka (2018b) discussed the relationship between affective variables (such as self-concept and beliefs about the nature of mathematics) and academic procrastination.

Therefore, the diachronic analysis of the research reports on STT in the 13 PME conferences shows a clear evolution toward a more holistic view of STT that increasingly includes socio-cultural and affective considerations.

3.2 STT in journal papers and book chapters

Following the selection criteria described in the method section, we obtained a corpus of 55 papers (Table 4). As hypothesised, we found several papers extending the ideas discussed by the authors in the international conferences presented in the previous section; therefore, the analysis of this corpus is particularly significant to gain a clear picture of the state of the art of STT research.

The data about the university affiliation of the authors and the geographical contexts where the studies were developed underlines again an issue of representation: the largest number of contributions comes from authors working in European universities reporting studies developed in Europe (63%). Research concerning other regions, such as South America, Asia, Africa, is almost completely absent in the identified corpus.

Concerning the analysis of the methods in the empirical studies, we found a balance between qualitative (43%) and quantitative (37%) approaches (20% used a mixed approach), as well as a variety of instruments and targets (summarised in Table 5).

In particular, the analysis of National School Standards or textbooks allows us to compare different contexts, leading to the awareness that the systems in school and university are culturally embedded (Frank & Thompson, 2021). To this aim, Vollstedt et al. (2014) elaborated a framework for analysing and comparing mathematics textbooks.

The analysis of the research methods highlights two related issues: most data are collected through online surveys (but the work by Geisler and Rolka (2021) represents a
Table 4  Journals and books: the complete list of selected publications

| Author(s)                  | Type of study | Method      | Sample and instruments                                                                 | Context                        |
|----------------------------|---------------|-------------|----------------------------------------------------------------------------------------|--------------------------------|
| Brandell et al. (2008)     | Empirical     | Qualitative | Analysis of official curricula                                                          | Sweden                         |
| Clark and Lovric (2008)    | Theoretical   | –           | –                                                                                      | Australia, Canada              |
| Godfrey and Thomas (2008)  | Empirical     | Mixed       | Three groups of students: in the lower secondary school, upper secondary school, and first year at university | New Zealand                    |
| Tall (2008)                | Theoretical   | –           | –                                                                                      | UK                             |
| Clark and Lovric (2009)    | Theoretical   | –           | –                                                                                      | Australia, Canada              |
| Hong et al. (2009)         | Empirical     | Quantitative| 178 schoolteachers, 26 lecturers (questionnaire, interview) in New Zealand             | Thailand, New Zealand          |
| Liston and O’Donoghue (2009)| Empirical     | Quantitative| 607 university students (questionnaire)                                                 | Ireland                        |
| Culpepper et al. (2010)    | Empirical     | Quantitative| 2.108 students (results in standardised test)                                           | USA                            |
| Engelbrecht (2010)         | Theoretical   | –           | –                                                                                      | South Africa                   |
| Liston and O’Donoghue (2010)| Empirical     | Qualitative | 15 university students (semi-structured interviews)                                     | Ireland                        |
| Hernandez-Martinez et al. (2011)| Empirical     | Qualitative | School teachers and managers (interview and observation of lessons)                    | UK                             |
| Klymchuk et al. (2011)     | Empirical     | Mixed       | 63 lecturers from 24 countries (questionnaire)                                         | New Zealand, Germany, Australia|
| Lithner (2011)             | Theoretical   | –           | –                                                                                      | Sweden                         |
| Bardelle and Di Martino (2012)| Didactical Design| – | –                                                                                      | Italy                          |
| Pampaka et al. (2012)      | Empirical     | Quantitative| University students (questionnaire)                                                   | UK                             |
| Selden (2012)              | Theoretical   | –           | –                                                                                      | USA                            |
| Thomas and Klymchuk (2012) | Empirical     | Mixed       | 178 schoolteachers, 26 lecturers (questionnaire, interview, observation of lessons)    | New Zealand                    |
| Varsavsky (2012)           | Empirical     | Quantitative| 1240 university students (students’ academic results)                                  | Australia                      |
| Adamuti-Trache et al. (2013)| Empirical     | Quantitative| 4,569 school students in USA over the 5-year period 2002–2006 (student gender, graduation year, high-school attended, performance in first year) | Canada, USA                    |
| Daza et al. (2013)         | Didactical Design| – | –                                                                                      | Spain                          |
| Gueudet (2013)             | Theoretical   | –           | –                                                                                      | France                         |
| Hernandez-Martinez and Williams (2013)| Empirical | Qualitative | 2 university students (narratives)                                                    | UK                             |
| Author(s)               | Type of study | Method       | Sample and instruments                                                                                                                                                                                                 | Context            |
|------------------------|---------------|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------|
| Duah et al. (2014)     | Empirical     | Mixed        | Observation of 8 peer-assisted learning sessions                                                                                                                                                                          | UK                 |
| Pepin (2014a)          | Empirical     | Mixed        | 1 university student in UK (interview with student and his teachers/lecturers, documents from the school and the university of the student)                                                                                       | Norway             |
| Pepin (2014b)          | Empirical     | Qualitative  | 1 university student in UK (interview with student and his teachers/lecturers, documents from the school and the university of the student)                                                                                       | Norway             |
| Vollstedt et al. (2014)| Theoretical   | –            | –                                                                                                                                                                                                                      | Germany            |
| Hong and Thomas (2015) | Empirical     | Mixed        | 136 university students in Korea (students’ scripts)                                                                                                                                                                     | Korea, New Zealand|
| Hernandez-Martinez (2016)| Empirical   | Qualitative  | 2 university students (narratives)                                                                                                                                                                                        | UK                 |
| Jooganah and Williams (2016)| Empirical | Qualitative  | 8 university students, 12 lecturers (interviews)                                                                                                                                                                           | UK                 |
| Bengmark et al. (2017) | Empirical     | Quantitative | 361 university students (2 questionnaires)                                                                                                                                                                                  | Sweden             |
| Corriveau (2017)       | Empirical     | Qualitative  | 3 schoolteachers, 3 lecturers (teachers’ scripts)                                                                                                                                                                           | Canada             |
| Corriveau and Bednarz (2017)| Empirical | Qualitative  | 3 schoolteachers, 3 lecturers (verbatim transcriptions of the meetings: 36 h)                                                                                                                                              | Canada             |
| Jablonka et al. (2017) | Empirical     | Qualitative  | 60 university students in Sweden (interview)                                                                                                                                                                                | UK, Sweden         |
| Rach and Heinze (2017) | Empirical     | Quantitative | 182 university students (questionnaire, students’ scripts from a test)                                                                                                                                                      | Germany            |
| Ufer et al. (2017)     | Empirical     | Quantitative | 323 university students (questionnaire)                                                                                                                                                                                   | Germany            |
| Burazin and Lovric (2018)| Theoretical  | –            | –                                                                                                                                                                                                                      | Canada             |
| Hausberger (2018)      | Theoretical   | –            | –                                                                                                                                                                                                                      | France             |
| Kouvela et al. (2018)  | Empirical     | Qualitative  | 10 university students, 42 lecturers (observation of lessons, questionnaire, interview)                                                                                                                                   | UK                 |
| Thoma and Nardi (2018) | Empirical     | Qualitative  | 22 university students (students’ scripts from the final examination)                                                                                                                                                     | UK                 |
| Di Martino and Gregorio (2019)| Empirical | Qualitative  | 127 university students (questionnaire, interview)                                                                                                                                                                         | Italy              |
| Dibbs (2019)           | Empirical     | Qualitative  | 8 university students (interview)                                                                                                                                                                                          | USA                |
| Author(s)                          | Type of study | Method     | Sample and instruments                                                                 | Context               |
|-----------------------------------|---------------|------------|----------------------------------------------------------------------------------------|-----------------------|
| Koichu and Pinto (2019)           | Theoretical   | –          | –                                                                                      | Israel                |
| Kosiol et al. (2019)              | Empirical     | Quantitative | 120 students (school qualification grade, test results, questionnaire, exam scores)    | Germany               |
| Lyakhova and Neate (2019)         | Empirical     | Quantitative | 236 university students (questionnaire, interview, school results)                     | UK (Wales)            |
| Schüler-Meyer (2019)              | Empirical     | Qualitative | 15 school students in Germany (videotape of the lessons)                               | The Netherlands       |
| Sommerhoff and Ufer (2019)        | Empirical     | Quantitative | 114 school students, 66 university students, 273 mathematicians (questionnaire)       | Germany               |
| Deeken et al. (2020)              | Empirical     | Qualitative | 952 lecturers (questionnaire)                                                         | Germany               |
| Gueudet and Thomas (2020)         | Theoretical   | –          | –                                                                                      | France, New Zealand   |
| Rach and Ufer (2020)              | Empirical     | Quantitative | 1553 university students (test results)                                               | Germany               |
| Artigue (2021)                    | Theoretical   | –          | –                                                                                      | France                |
| Frank and Thompson (2021)         | Empirical     | Quantitative | 356 university students (students’ production, analysis of precalculus textbooks)     | USA                   |
| Geisler and Rolka (2021)          | Empirical     | Quantitative | 104 universities students (paper and pencil questionnaire)                            | Germany               |
| Ghedamsi and Lecorre (2021)       | Empirical     | Mixed      | 57 university teachers in Tunisia (questionnaire, observation of lessons, analysis of calculus text) |
| Hochhuth et al. (2021)            | Theoretical   | –          | –                                                                                      | Germany, Canada, UK   |
| O’Shea and Breen (2021)           | Empirical     | Qualitative | 10 university students (semi-structured interviews)                                   | Ireland               |
recent exception) and the sample is almost exclusively a sample of volunteers. This latter aspect, recurrent in the mathematics education research, appears to be particularly relevant in STT research since it involves adults, asking them to report an event often perceived as a personal failure.

### 3.3 Theoretical models

The 55 selected papers include a great variety of theoretical frameworks: several of these theoretical approaches are related to Tall’s ideas of advanced mathematical thinking and the three worlds of mathematics (e.g., Deeken et al., 2020; Hong et al., 2009), others are based on the Anthropological Theory of the Didactic (e.g., Hausberger, 2018), and others are within the theory of commognition by Sfard (2008). In the latter case, the focus is on the shift of mathematical discourses between secondary school and university (Thoma & Nardi, 2018).

Recently, more authors have adopted frameworks related to affective constructs not originally developed in the field of STT: Hernandez-Martinez et al. (2011) focused on mathematical identity adopting the perspective of Sfard and Prusak (2005); Ufer et al. (2017) conceptualised interest within the person-object theory of interest by Krapp (2002); Dibbs (2019) used engagement theory (Fredricks et al., 2004) to study students’ affective reactions to failure in a calculus course; Geisler (2021) analysed the role of attitude in the dropout from university mathematics within the three-dimensional model of attitude (Di Martino & Zan, 2010).

In 2008, Clark and Lovric observed that ‘perhaps the most notable feature of the existing body of research on transition is the absence of a theoretical model’ (p. 25). In a special issue of the *Mathematics Education Research Journal* dedicated to transitions, two specific (and influential) models were discussed: the three worlds of mathematics by Tall (2008) and the rite of passage by Clark and Lovric (2008).

The three worlds of Mathematics is a theory about the development of mathematical thinking that Tall presented at PME in Bergen (Tall, 2004). In this theory, the development of mathematical thinking is described as the development of perceptions of three different but interrelated worlds. In 2008, Tall used this theory to focus on the changes in thinking involved in the STT and on the individual development needed for this transition. According to this theoretical model, there are three fundamental mental structures that shape long-term learning and mathematical thinking: recognition of patterns, repetition of sequences of actions, and language. In this cognitive and epistemological perspective, Tall (2008) identified ‘three worlds of mathematics that develop in sophistication in quite different ways’ (p. 7): conceptual embodiment, proceptual symbolism (APOS theory is included in this world), and axiomatic formalism. Tall explained how, in his view, the

| Target          | Instruments and indicators                                                                 |
|-----------------|---------------------------------------------------------------------------------------------|
| Students        | Prompts in mathematical tasks, questionnaires, biographical and structured interviews, Likert scales, journals, school results, academic results |
| School teachers | Questionnaires, interviews, direct observations                                               |
| Lecturers       | Questionnaires, interviews, direct observations                                               |
| Other targets:  | National School Standards, textbooks                                                          |
blending of embodiment and symbolism gives a more accurate way of developing sophistication in mathematical thinking. In the final version of his theoretical model, Tall (2013) included an affective dimension recognising the role of emotions in the interpretation of previous experiences with mathematics, and therefore in the individual development of mathematical thinking.

Clark and Lovric (2008) adapted a well-established anthropological theory to the study of STT: that of rites of passage. This model recognised three stages in STT (Fig. 2).

The liminal stage includes the period from the last part of high school to the first part of university. It is characterised by an unavoidable crisis, known mathematical routines are challenged, and first year students need to find their place in a new mathematics community. This model appeared initially strongly influenced by the cognitive perspective in STT; Clark and Lovric (2008) discussed only the cognitive shock of the passage from informal to formal language and reasoning in mathematics. A year later, Clark and Lovric (2009) recognised that the rite of passage inevitably leads to the emergence of affective reactions: the initial reaction of euphoria, the feelings of inadequacy during the crisis, and the recovery after the resolution of the crisis. These affective reactions are particularly strong for those students who were successful in secondary school: this is the case of most of the first-year students in mathematics (Di Martino & Gregorio, 2019).

The rite of passage model has two main implications. First, dealing with a significant crisis is a necessary step for a successful passage: instead of avoiding the crisis — for example making the new context like the old one — the crisis needs to be understood to offer students support to overcome it. As Thomas and Klymchuk (2012) observed: ‘the existence of demanding aspects of transition that are difficult to control is not in itself a good enough reason to ignore those that can be managed to produce a better experience for students’ (p. 285). An unsuccessful rite of passage may result in a never completed incorporation stage, and students’ dropout can be interpreted in this perspective. Second, the rite of passage model stresses the fact that socio-cultural aspects cannot be disregarded in the analysis of STT: the old and new communities through which the rite of passage is accomplished are context specific.

### 3.4 Main themes of research

Through the coding process, we identified, inductively, four main research themes. We describe them in turn below.

1. The mathematical gap between secondary school and university. This gap is described in terms of students’ thinking (Godfrey & Thomas, 2008), approach and content (Brandell et al., 2008), acceptance criteria for justification (Selden, 2012; Sommerhoff & Ufer, 2019) and for legitimate mathematical activity (Jablonka et al., 2017), teaching style and assessment (Thomas & Klymchuk, 2012), didactic contract (Pepin, 2014b)
and messages students receive (Kouvela et al., 2018), identity (Jooganah & Williams, 2016), and high school calculus outcomes and university calculus requirements (Ghedamsi & Lecorre, 2021). These studies are mainly conducted within a socio-cultural perspective, adopting the three worlds of mathematics framework (Tall, 2008). In recent years, the approach to STT has become more holistic, including new viewpoints. For example, some studies consider the social and discursive perspective related to the analysis of commognitive conflicts (Thoma & Nardi, 2018); others describe the gap between school and university mathematical experiences through the description of the perception of the main actors involved: students (e.g., Hernandez-Martinez et al., 2011; O’Shea and Breen, 2021), schoolteachers (Hong et al., 2009), lecturers (Klymchuk et al., 2011; Deeken et al., 2020), or compare these different perceptions (Corriveau, 2017).

(2) The potential of technology to facilitate the STT. Two issues emerge within this category: the effective use of CAS (Computer Algebra Systems) in STT (Hong & Thomas, 2015; Varsavsky, 2012) and the analysis of the potential of ICT (Information and Communication Technology) to facilitate the STT (Bardelle & Di Martino, 2012; Daza et al., 2013). It is interesting to observe that these kinds of studies are limited to the period 2012–2015: the recent events related to the pandemic could (should?) generate new interest towards this line of research in STT (Chan et al., 2021).

(3) The factors correlated with academic success. The studies in this category consider a wide range of cognitive, social, and affective factors and are mostly quantitative, involving large samples. Their explicit goal is to highlight significant correlations between academic success and other factors, such as students’ attitudes (Geisler, 2021), standardised test results (Culpepper et al., 2010), attended secondary school (Adamut-Trache et al., 2013), prior knowledge (Rach & Ufer, 2020), students’ learning prerequisites (Rach & Heinze, 2017), interest (Kosiol et al., 2019), and students’ beliefs (Geisler & Rolka, 2021).

(4) Failure in STT. This category represents studies of failure to transition: they are mostly qualitative, based on the collection of narratives, often framed as case studies (Hernandez-Martinez, 2016). The shared assumption of these studies is that the difficulties in STT are inevitable — according to Clark and Lovric (2009) even essential — and there is a thin line between success and failure. The description and interpretation of the failure is considered a significant key to understand, prevent, and overcome the students’ difficulties in STT. The definition of failure in STT varies in these studies: there is a local meaning, i.e., negative results in some first-year university exam (Dibbs, 2019) and a global meaning, i.e., students who leave university studies (Di Martino & Gregorio, 2019).

These four themes of research are highly specific to mathematics. This is evident for the first two themes which deal with subject-related issues. However, it is also the case for the latter two themes. Regarding the third theme, the factors considered are mathematics-related: for example, students’ beliefs and attitudes reveal students’ perceptions about the nature of the mathematics they are encountering at university. The fourth theme, that of failure/success in STT, is related to the students’ vision of the nature of mathematics. A change in one’s mathematical theory of failure/success is a change in one’s vision of mathematics. The mathematics epistemology conveyed by the mathematical culture in the new university environment affects students’ mathematical theories of success through
the introduction of new mathematical symbols, knowledge, customs, and requirements for success. Therefore, all the elements of difficulty, not only the cognitive ones, but also the affective and sociocultural ones, are highly specific to mathematics.

4 Conclusion and directions for research

First, a meta-reflection about literature searches based on fully automated search engines such as Google Scholar. Such searches not only present an issue of non-reproducibility (Gusenbauer & Haddaway, 2020) but also present an issue of control (or rather of poor control). These searches are affected by external and contextual factors. The list produced is based on an unknown ranking algorithm (Beel & Gipp, 2009) and the profiling process and geolocation of who develops the search also play a role. The introduction of external selection criteria not fully controlled by researchers is a significant dilemma for the scientific community.

Notwithstanding this significant issue, the academic search engines are an essential resource to develop systematic literature reviews. We believe that adopting the recommendations of Haddaway et al. (2015) — for example using a primary and a supplementary search engine, adopting a suitable search query, and considering a large sample of the papers — it is possible to obtain a representative picture of the state of the art in the field investigated, also highlighting the so called ‘grey literature’ (Haddaway et al., 2015).

Our review of the research literature on STT from 2008 to 2021 highlights the variety of theoretical frameworks in use, the growing awareness of the complexity of phenomena at play in STT and the consequent adoption of a more holistic approach to STT that goes beyond a purely cognitive interpretation, including socio-cultural and affective issues. The first studies focused on the cognitive and epistemological obstacles of the shift toward advanced mathematical thinking have been integrated and complemented by studies considering social, cultural, and affective issues in the last decade. On the other hand, Artigue (2021) recently underlined how ‘the socio-cultural turn... has not yet impacted research’ (p. 9) at university level and we argue that the ‘affective turn’ has also not been completely fulfilled in STT research.

The research results obtained considering social, cultural, and affective issues have already some clear implications for the teaching and learning of mathematics at secondary school and at university level. Since the seminal work of Tall (1991), we know much about the difference between tertiary mathematics and secondary school mathematics: mathematics is understood and presented in a different (advanced) way at the university level. The more recent research on the STT highlights how tertiary transition involves other changes than the purely cognitive and other actors. Many difficulties the learners experience in the passage from school mathematics to university mathematics appear to be related to a sudden change in their mathematics identity (Hernandez-Martinez et al., 2011). Many successful students develop a different view of mathematics in their passage to university, often perceiving that their ability in mathematics is suddenly reduced and, consequently, developing very strong negative emotions in their university experience (Geisler & Rolka, 2021). This affective phenomenon is however related to an epistemological aspect: the meaning of being a successful student in mathematics. The individuals’ theory of success in mathematics are rooted and consolidated during the school experience (Di Martino & Zan, 2010), going often into crisis during the tertiary transition. Whether the development of the students’ theories of success during STT is unavoidable and related to the
epistemology of the advanced mathematics encountered at university is an open question at the boundary between epistemological and didactical issues.

Concerning the second research question we posed, we identified four main themes of the STT research: the mathematical gap between secondary school and university, the potential of technology to facilitate STT, and the factors correlated to academic success and to academic failure in STT. These strands of research produced significant outcomes. However, we believe that more research is needed to improve our understanding of the relationship between cognitive, affective, social, and cultural aspects of the STT. We encourage studies that consider the dynamic nature of STT — that consider STT as a process — and bring into play the cultural context in which this crisis takes place. In this perspective, comparative studies between cultural or institutional contexts are still rare: an interesting exception is represented by the study of Deeken et al. (2020) that, through the Delphi method, described which students’ mathematical abilities are considered minimal prerequisites by university mathematics lecturers. Studies involving and comparing several institutions or countries are rare (Di Martino et al., 2022, is one such example), but much needed, since they can help to understand the role of contextual factors and the generalisability of studies conducted in a specific context. Further studies in this direction would surely represent a valuable addition to the current body of research.

From a methodological point of view, the analysis of existing research highlights on the one hand the use of several different instruments, approaches, and samples. On the other hand, it points to two significant issues. First, most data are collected through online surveys: this choice is ‘not neutral’. Psychologist have discussed the impact of computer versus paper–pencil survey in collecting self-reports (Bates & Cox, 2008) and, in mathematics education, recent publications address the impact in students’ performance in online versus pen and paper tasks (Lemmo, 2021).

Second, the participants of these studies are almost exclusively volunteers, and we need to consider and discuss the limitations related to this. The effects of a sample of volunteers appear to be particularly significant in the analysis of failure in STT, where students who drop out or are about to do so are often the focus of research. The volunteer sampling in the STT may create a bias towards higher achieving students (Vollstedt et al., 2014).

In our overview, we included papers such as Doukhan (2020), Griese (2017), Jablonka et al. (2017), and Hong and Thomas (2015). Those papers focus on STT concerning non-specialist students: i.e., students who study mathematics as part of their degree but are not enrolled in a degree course in mathematics. The study of the differences in the mathematical transition to the various STEM degrees — the differences in the mathematical transition between specialist and non-specialist students — appears to be a significant perspective for further research.

These differences can be related to the different mathematical identities of the first-year students, to the different degrees of discontinuity of mathematical contents (for example, calculus) as they are presented at school and as they are presented in the different degrees, as well as to the different mathematical practices and requests in the different degrees. In our view, this research should also involve epistemological, socio-cultural, and affective aspects.

Finally, the result of our systematic review confirms a need of our community: that of learning more about STT in the areas of the world that are not represented in our final corpus. This is not only an important issue of equity and participation, but — considering the role of cultural, affective, and social factors in the STT — our limited knowledge of many educational contexts signifies a limited understanding of the STT, an understanding too culturally bound. We firmly believe that the mathematics education community should
make all possible efforts to support researchers from underrepresented educational contexts interested in developing research about STT.

Funding Open access funding provided by Università di Pisa within the CRUI-CARE Agreement.

Data availability The datasets analysed during the current study are available from the correspondent author upon reasonable request. These datasets were derived from the following public domain resources: Google Scholar and ERIC.

Declarations

Conflict of interest The authors declare no competing interests.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

References

Adamuti-Trache, M., Bluman, G., & Tiedje, T. (2013). Student success in first-year university physics and mathematics courses: Does the high-school attended make a difference? International Journal of Science Education, 35(17), 2905–2927. https://doi.org/10.1080/09500693.2012.667168

Adkins, M., & Noyes, A. (2016). Reassessing the economic value of advanced level mathematics. British Educational Research Journal, 42(1), 93–116. https://doi.org/10.1002/berj.3219

Artigue, M. (2016). Mathematics education research at university level: Achievements and challenges. In E. Nardi, C. Winslow & T. Hausberger (Eds.), Proceedings of the first conference of the international network for didactic research in university mathematics (pp. 11–27). University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01337874/document.

Artigue, M. (2021). Mathematics education research at university level: Achievements and challenges. In V. Durand-Guerrier, R. Hochmuth, E. Nardi, & C. Winsløw (Eds.), Research and development in university mathematics education (pp. 3–21). Routledge. https://doi.org/10.4324/9780429346859

Bakker, A., Cai, J., & Zenger, L. (2021). Future themes of mathematics education research: An international survey before and during the pandemic. Educational Studies in Mathematics, 107, 1–24. https://doi.org/10.1007/s10649-021-10049-w

Bampili, A., Charalampos, S., & Zachariades, T. (2018). The transition from high school to university mathematics: Entering a new community of practice. In E. Bergqvist, M. Österholm, C. Granberg, & L. Sumpter (Eds.), Proceedings of the 42nd conference of the international group for the psychology of mathematics education (Vol. 2, pp. 115–122). PME.

Bardelle, C., & Di Martino, P. (2012). E-learning in secondary–tertiary transition in mathematics: For what purpose? ZDM-Mathematics Education, 44, 787–800. https://doi.org/10.1007/s11858-012-0417-y

Bates, S., & Cox, J. (2008). The impact of computer versus paper–pencil survey, and individual versus group administration, on self-reports of sensitive behaviors. Computers in Human Behavior, 24(3), 903–916. https://doi.org/10.1016/j.chb.2007.02.021

Beel, J., & Gipp. B. (2009). Google Scholar’s ranking algorithm: An introductory overview. In B. Larsen, & J. Leta (Eds.), Proceedings of 12th international conference on scientometrics and informetrics (Vol. 1, pp. 230–241). Retrieved September 30, 2022, from http://www.issi-society.org/proceedings/issi_2009/ISSI2009-proc-vol1_Aug2009_batch2-paper-1.pdf.

Beitlich, J., Obersteiner, A., Moll, G., Mora Ruano, J., Pan, J., Reinhold, S., & Reiss, K. (2014). The role of pictures in reading mathematical proofs: An eye movement study. In P. Liljedahl, S. Oesterle, C. Nicol, & D. Allan (Eds.), Proceedings of the 38th conference of the international group for the
psychology of mathematics education and the 36th conference of the north American chapter of the psychology of mathematics education (Vol. 2, pp. 121–128). PME.

Bengmark, S., Thunberg, H., & Winberg, T. (2017). Success-factors in transition to university mathematics. *International Journal of Mathematical Education in Science and Technology*, 48(7), 988–1001. https://doi.org/10.1080/0020739X.2017.1310311

Bergsten, C., & Jablonka, E. (2019). Understanding the secondary-tertiary transition in mathematics education: Contribution of theories to interpreting empirical data. In U. Jankvist, M. Van den Heuvel-Panhuizen, & M. Veldhuis (Eds.), *Proceedings of the eleventh congress of the european society for research in mathematics education*. Utrecht University. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-02422577.

Bloch, I., & Gibel, P. (2016). A model to analyse the complexity of calculus knowledge at the beginning of university course. In E. Nardi, C. Winsløw & T. Hausberger (Eds.), *Proceedings of the first conference of the international network for didactic research in university mathematics* (pp. 477–486). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849952/document.

Brandell, G., Hemmi, K., & Thunberg, H. (2008). The widening gap — A Swedish perspective. *Mathematics Education Research Journal*, 20, 38–56. https://doi.org/10.1007/BF03217476

Brandes, H., & Hardy, N. (2018). From single to multi-variable calculus: A transition? In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M. Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 487–496). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849952/document.

Broley, L., & Hardy, N. (2018). A study of transitions in an undergraduate mathematics program. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M. Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 487–496). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849952/document.

Brousseau, G. (2002). Theory of didactical situations in mathematics. *Springer*. https://doi.org/10.1007/0-306-47211-2

Burazin, A., & Lovric, M. (2018). Transition from secondary to tertiary mathematics: Culture shock — Mathematical symbols, language, and reasoning. In A. Kajander, J. Holm, E. Chernoff (Eds.), *Teaching and learning secondary school mathematics. Advances in mathematics education* (pp. 601–611). Springer. https://doi.org/10.1007/978-3-319-92390-1_55

Chan, M., Sabena, C., & Wagner, D. (2021). Mathematics education in a time of crisis — A viral pandemic. *Educational Studies in Mathematics*, 108, 1–13. https://doi.org/10.1007/s10649-021-10113-5

Chevallard, Y. (1992). Fundamental concepts in didactics: Perspectives provided by an anthropological approach. In R. Douady & A. Mercier (Eds.), *Research in didactique of mathematics, selected papers* (pp. 131–168). La Pensée Sauvage.

Clark, M., & Lovric, M. (2008). Suggestion for a theoretical model for secondary-tertiary transition in mathematics. *Mathematics Education Research Journal*, 20(2), 25–37. https://doi.org/10.1007/BF03217475

Clark, M., & Lovric, M. (2009). Understanding secondary–tertiary transition in mathematics. *International Journal of Mathematical Education in Science and Technology*, 40(6), 755–776. https://doi.org/10.1080/00207390902912878

Cohen, L., Manion, L., & Morrison, K. (2007). Research methods in education. *Routledge Falmer*. https://doi.org/10.4324/9780203029053

Corriveau, C. (2017). Secondary–to-tertiary comparison through the lens of ways of doing mathematics in relation to functions: A study in collaboration with teachers. *Educational Studies in Mathematics*, 94, 139–160. https://doi.org/10.1007/s10649-016-9719-2

Corriveau, C., & Bednarz, N. (2017). The secondary-tertiary transition viewed as a change in mathematical cultures: An exploration concerning symbolism and its use. *Educational Studies in Mathematics*, 95, 1–19. https://doi.org/10.1007/s10649-016-9738-z

Culpepper, S., Basile, C., Ferguson, C., Lanning, J., & Perkins, M. (2010). Understanding the transition between high school and college mathematics and science. *Journal of Mathematics and Science, 12*(1), 157–167. https://doi.org/10.25891/EGS9-B282

Dahl, B. (2009). Transition problems in mathematics that face students moving from compulsory through to tertiary level education in Denmark: Mismatch of competencies and progression. In M. Tzekaki, M. Kaldrimidou, & H. Sakonidis (Eds.), *Proceedings of the 33rd conference of the
Daza, V., Makriyannis, N., & Riera, C. (2013). MOOC attack: Closing the gap between pre-university and university mathematics. Open Learning: The Journal of Open, Distance and e-Learning, 28(3), 227–238. https://doi.org/10.1080/02680513.2013.872558

De Guzman, M., Hodgson, B. R., Robert, A., & Villani, V. (1998). Difficulties in the passage from secondary to tertiary education. In G. Fischer (Ed.), Documenta mathematica: Proceedings of the international congress of mathematicians, Extra volume (pp. 747–762). Gemono. Retrieved September 30, 2022, from https://www.ime.usp.br/~vhgiusti/dificuldades_passagem.pdf

Deeken, C., Neumann, I., & Heinze, A. (2020). Mathematical prerequisites for STEM programs: What do university instructors expect from new STEM undergraduates? International Journal of Research in Undergraduate Mathematics Education, 6, 23–41. https://doi.org/10.1007/s40753-019-00098-1

Di Martino, P., & Maracci, M. (2009). The secondary-tertiary transition: Beyond the purely cognitive. In M. Tzekaki, M. Kaldrimidou, & H. Sakonidis (Eds.), Proceedings of the 33rd conference of the international group for the psychology of mathematics education (Vol. 2, pp. 401–408). PME.

Di Martino, P., & Zan, R. (2010). ‘Me and maths’: Towards a definition of attitude grounded on students’ narratives. Journal of Mathematics Teacher Education, 13, 27–48. https://doi.org/10.1007/s10857-009-9134-z

Di Martino, P., & Gregorio, F. (2018). The first-time phenomenon: Successful students’ mathematical crisis in secondary-tertiary transition. In E. Bergqvist, M. Osterholm, C. Granberg, & L. Sumper (Eds.), Proceedings of the 42nd conference of the international group for the psychology of mathematics education (Vol. 2, pp. 339–346). PME.

Di Martino, P., & Gregorio, F. (2019). The mathematical crisis in secondary-tertiary transition. International Journal of Science and Mathematics Education, 17, 825–843. https://doi.org/10.1007/s10763-018-9894-y

Di Martino, P., Gregorio, F., & Iannone, P. (2022). Transition from school to university mathematics: A crisis ‘in context.’ Educational Studies in Mathematics. https://doi.org/10.1007/s10649-022-10179-9

Dias, M., Artigue, M., Jahn, A., & Campos, T. (2010). A comparative study of the secondary-tertiary transition. In M. Pinto, & T. Kawasaki (Eds.), Proceedings of the 34th conference of the international group for the psychology of mathematics education (Vol. 2, pp. 129–136). PME.

Dibbs, R. (2019). Forged in failure: Engagement patterns for successful students repeating calculus. Educational Studies in Mathematics, 101, 35–50. https://doi.org/10.1007/s10649-019-9877-0

Doukhan, C. (2020). Mathematical modelling in probability at the secondary-tertiary transition, example of biological sciences students at university. In T. Hausberger, M. Bosch, & F. Chellougui (Eds.), Proceedings of the third conference of the international network for didactic research in university mathematics (pp. 123–132). University of Carthage and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-03113847/document.

Duah, F., Croft, T., & Inglis, M. (2014). Can peer assisted learning be effective in undergraduate mathematics? International Journal of Mathematical Education in Science and Technology, 45(4), 552–565. https://doi.org/10.1080/0020739X.2013.855329

Dubinsky, E. (1991). Reflective abstraction in advanced mathematical thinking. In D. Tall (Ed.), Advanced Mathematical Thinking, 95–123. Kluwer. https://doi.org/10.1007/0-306-47203-1_7

Durand-Guerrier, V., Hochmuth, R., Goodchild, S., & Hogstad N. (Eds.) (2018). Proceedings of the second conference of the international network for didactic research in university mathematics. University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/INDRUM2018/public/Indrum2018Proceedings.pdf

Durand-Guerrier, V., Hochmuth, R., Nardi, E., & Winsløj, C. (Eds.) (2021). Research and development in university mathematics education. Routledge. https://doi.org/10.4324/9780429346859

Engelbrecht, J. (2010). Adding structure to the transition process to advanced mathematical activity. International Journal of Mathematical Education in Science and Technology, 41(2), 143–154. https://doi.org/10.1080/00207390903391890

Flores González, M., Vandebruck, F., & Vivier, L. (2020). Suites définies par récurrence dans la transition lycée-université: Activité et travail mathématique. In T. Hausberger, M. Bosch, & F. Chellougui (Eds.), Proceedings of the third conference of the international network for didactic research in university mathematics (pp. 83–92). University of Carthage and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-03113856/document

Frank, K., & Thompson, P. (2021). School students’ preparation for calculus in the United States. ZDM-Mathematics Education, 53, 549–562. https://doi.org/10.1007/s11858-021-01231-8
Fredricks, J., Blumenfeld, P., & Paris, A. (2004). School engagement: Potential of the concept, state of the evidence. *Review of Educational Research, 74*(1), 59–109. https://doi.org/10.3102/003465430740010159

Geisler, S., & Rach, S. (2019). Interest development and satisfaction during the transition from school to university. In M. Graven, H. Venkat, A. Essien, & P. Vale (Eds.), *Proceedings of the 43rd conference of the international group for the psychology of mathematics education* (Vol. 2, pp. 264–271). PME.

Geisler, S., & Rolka, K. (2018a). Affective variables in the transition from school to university mathematics. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 507–516). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849967/document.

Geisler, S., & Rolka, K. (2018b). Academic procrastination in the transition from school to university mathematics. In E. Bergqvist, M. Österholm, C. Granberg, & L. Sumpter (Eds.), *Proceedings of the 42nd conference of the international group for the psychology of mathematics education* (Vol. 2, pp. 451–458). PME.

Geisler, S., & Rolka, K. (2021). “That wasn’t the math I wanted to do!”—Students’ beliefs during the transition from school to university mathematics. *International Journal of Science and Mathematics Education, 19*, 599–618. https://doi.org/10.1007/s11676-020-10072-y

Geisler, S. (2021). Early dropout from university mathematics: The role of students’ attitudes towards mathematics. In M. Improasthi, N. Changsri & N. Boonessa (Eds.), *Proceedings of the 44th conference of the international group for the psychology of mathematics education* (Vol. 2, pp. 320–329). PME.

Ghedamsi, I., & Lecorre, T. (2021). Transition from high school to university calculus: A study of connection. *ZDM-Mathematics Education, 53*, 563–575. https://doi.org/10.1007/s11858-021-01262-1

Godfrey, D., & Thomas, M. (2008). Student perspectives on equation: The transition from school to university. *Mathematics Education Research Journal, 20*, 71–92. https://doi.org/10.1007/BF03217478

Gradwohl, J., & Eichler, A. (2018). Predictors of performance in engineering mathematics. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N.M Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 25–134). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849947/document.

Green, B., Johnson, C., & Adams, A. (2006). Writing narrative literature reviews for peer reviewed journals: Secrets of the trade. *Journal of Chiropractic Medicine, 5*, 101–117. https://doi.org/10.1016/S0899-3467(07)60142-2

Griese, B. (2017). Learning strategies in engineering mathematics — Evaluation of a design research project. In B. Kaur, W. K. Ho, T. L. Toh & B. H. Choy (Eds.), *Proceedings of the 41st conference of the international group for the psychology of mathematics education* (Vol. 2, pp. 361–368). PME.

Gueudet, G. (2008). Investigating the secondary–tertiary transition. *Educational Studies in Mathematics, 67*, 237–254. https://doi.org/10.1007/s10649-007-9100-6

Gueudet, G., Bosch, M., DiSessa, A., Nam Kwon, O., & Verschaffel, L. (2016). Transitions in mathematics education. *Springer*. https://doi.org/10.1007/978-3-319-31622-2

Gueudet, G., & Pepin, B. (2016). Students’ work in mathematics and resources mediation at entry to university. In E. Nardi, C. Winsløw & T. Hausberger (Eds.), *Proceedings of the first conference of the international network for didactic research in university mathematics* (pp. 444–453). University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01310829/document.

Gueudet, G., & Pepin, B. (2017). Didactic contract and secondary–tertiary transition: A focus on resources and their use. In R. Göller, R. Biehler, R. Hochmuth & H. Rück (Eds.), *Proceedings of the KHM conference* (pp. 466–472). KHDM Report. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01310783/document.

Gueudet, G., & Thomas, M. (2020). Secondary–tertiary transition in mathematics education. In Lerman S. (Ed.), *Encyclopedia of mathematics education* (2nd ed., pp. 762–766). Springer. https://doi.org/10.1007/978-3-030-15789-0_100026

Gueudet, G. (2013). Why is university mathematics difficult for students? Solid findings about the secondary–tertiary transition. *Newsletter of the European mathematical society* (pp. 46–48). Retrieved September 30, 2022, from https://www.euro-math-soc.eu/ems_education/Secondary_Tertiary.pdf

Gusenbauer, M., & Haddaway, N. (2020). Which academic search systems are suitable for systematic reviews or meta-analyses? Evaluating retrieval qualities of Google Scholar, PubMed, and 26 other resources. *Research Synthesis Methods, 11*, 181–217. https://doi.org/10.1002/jrsm.1378
Halverscheid, S., Pustelnik, K. (2013). Procedural and conceptual knowledge in calculus before entering the university: A comparative analysis of different degree courses. In K. Beswick, T. Muir & J. Wells (Eds.), Proceedings of the 39th conference of the international group for the psychology of mathematics education (Vol. 3, pp. 17–24). PME.

Hausberger, T. (2016). A propos des praxéologies structuralistes en Algèbre Abstraite. In E. Nardi, C. Winslòw & T. Hausberger (Eds.), Proceedings of the first conference of the international network for didactic research in university mathematics (pp. 296–305). University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01322982/document.

Hausberger, T. (2018). Structuralist praxeologies as a research program on the teaching and learning of abstract algebra. International Journal of Research in Undergraduate Mathematics, 4, 74–93. https://doi.org/10.1007/s40753-017-0063-4

Hausberger, T., Bosch, M., & Chellougui, F. (Eds.), (2020). Structuralist praxeologies as a research program on the teaching and learning of abstract algebra. Routledge. https://doi.org/10.4324/9780429346859

Hochmuth, R., Broley, L., & Nardi, E. (2021). Transitions to, across and beyond university. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M. Hogstad (Eds.), Proceedings of the second conference of the international network for didactic research in university mathematics (pp. 517–526). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/INDRUM2020/public/INDRUM2020_Proceedings.pdf.

Hernandez-Martinez, P. (2016). Lost in transition: Alienation and drop out during the transition to mathematically demanding subjects at university. International Journal of Educational Research, 79, 231–239. https://doi.org/10.1016/j.ijer.2016.02.005

Hernandez-Martinez, P., Williams, J., Black, L., Davis, P., Pampaka, M., & Wake, G. (2011). Students’ views on their transition from school to college mathematics: Rethinking ‘transition’ as an issue of identity. Research in Mathematics Education, 13(2), 119–130. https://doi.org/10.1080/14794802.2011.585824

Hernandez-Martinez, P., & Williams, J. (2013). Against the odds: Resilience in mathematics students in transition. British Educational Research Journal, 39(1), 45–59. Retrieved September 30, 2022, from http://www.jstor.org/stable/24464801.

Higher Education Statistics Agency. (2018). Retrieved September 30, 2022, from https://www.hesa.ac.uk/news/18-06-2020/sb257-higher-education-outcomes-statistics/study

Hochmuth, R., Broley, L., & Nardi, E. (2021). Transitions to, across and beyond university. In V. Durand-Guerrier, R. Hochmuth, E. Nardi, & C. Winslòw (Eds.), Research and development in university mathematics education (pp. 193–215). Routledge. https://doi.org/10.4324/9780429346859

Hochmuth, R. (2018). Discussing mathematical learning and mathematical praxeologies from a subject scientific perspective. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M. Hogstad (Eds.), Proceedings of the second conference of the international network for didactic research in university mathematics (pp. 517–526). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849940/document

Hong, Y., & Thomas, M. (2015). Graphical construction of a local perspective on differentiation and integration. Mathematics Educational Research Journal, 27, 183–200. https://doi.org/10.1007/s13394-014-0135-6

Hong, Y., Kerr, S., Klymchuk, S., McHardy, J., Murphy, P., Spencer, S., Thomas, M., & Watson, P. (2009). A comparison of teacher and lecturer perspectives on the transition from secondary to tertiary mathematics education. International Journal of Mathematical Education in Science and Technology, 40(7), 877–889. https://doi.org/10.1080/00207390903223754

Hong, Y., & Thomas, M. (2013). Graphical construction of a local perspective. In A. Lindmeier, & A. Heinze (Eds.), Proceedings of the 37th conference of the international group for the psychology of mathematics education (Vol. 3, pp. 81–90). PME.

Jablonska, E., Ashjari, H., & Bergsten, C. (2017). “Much palaver about greater than zero and such stuff” — First year engineering students’ recognition of university mathematics. International Journal of Research in Undergraduate Mathematics Education, 3, 69–107. https://doi.org/10.1007/s40753-016-0037-y

Jeschke, C., Neumann, L., & Heinze, A. (2016). Predicting early dropout from university mathematics: A measure of mathematics-specific academic buoyancy. In C. Csíkos, A. Rausch & J. Szitányi (Eds.), Proceedings of the 40nd conference of the international group for the psychology of mathematics education (Vol. 3, pp. 43–50). PME.
Jooganah, K., & Williams, J. (2016). Contradictions between and within school and university activity systems helping to explain students’ difficulty with advanced mathematics. *Teaching Mathematics and Its Applications, 35*(3), 159–171. https://doi.org/10.1093/teamat/hrw014

Khalloufi-Mouha, F. (2020). Analyse discursive de l’enseignement des fonctions trigonométriques dans la transition lycée/université. In T. Hausberger, M. Bosch, & F. Chellougui (Eds.), *Proceedings of the third conference of the international network for didactic research in university mathematics* (pp. 123–132). University of Carthage and INDRUM. Retrieved September 30, 2019, from https://hal.archives-ouvertes.fr/hal-03138844/document

Klymchuk, S., & Thomas, M. (2009). Teachers’ mathematical knowledge: The influence of attention. In M. Tzekaki, M. Kaldrimidou and H. Sakonidis (Eds.), *Proceedings of the 33rd conference of the international group for the psychology of mathematics education* (Vol. 3, pp. 361–368). University of Thessaloniki and PME.

Klymchuk, S., Gruenwald, N., & Jovanoski, Z. (2011). University lecturers’ views on the transition from secondary to tertiary education in mathematics: An international survey. *Mathematics Teaching Research Journal, 5*(1), 101–128.

Kock, Z. J., & Pepin, B. (2018). Student use of resources in calculus and linear Algebra. In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M. Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 336–345). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849945/document

Koichu B., & Pinto A. (2019). The secondary-tertiary transition in mathematics: What are our current challenges and what can we do about them? *Newsletter of the European Mathematical Society*. Retrieved September 30, 2022, from https://euro-math-soc.eu/sites/default/files/STT-survey-%2015-02-2019.pdf.

Kosiol, T., Rach, S., & Ufer, S. (2019). (Which) Mathematics interest is important for a successful transition to a university study program? *International Journal of Science and Mathematics Education, 17*, 1359–1380. https://doi.org/10.1007/s10763-018-9925-8

Kouvela, E., Hernandez-Martinez, P., & Croft, T. (2018). “This is what you need to be learning”: An analysis of messages received by first-year mathematics students during their transition to university. *Mathematics Education Research Journal, 30*, 165–183. https://doi.org/10.1007/s13394-017-0226-2

Kouvela, E., Hernandez-Martinez, P., & Croft, T. (2017). Secondary-tertiary transition: How messages transmitted by lecturers can influence students’ identities as mathematics learners? In B. Kaur, W. K. Ho, T. L. Toh & B. H. Choy (Eds.), *Proceedings of the 41st conference of the international group for the psychology of mathematics education* (Vol. 3, pp. 81–88). PME.

Krapp, A. (2002). Structural and dynamic aspects of interest development: Theoretical considerations from an ontogenetic perspective. *Learning and Instruction, 12*(4), 383–409. https://doi.org/10.1016/S0926-2091(01)00011-1

Lemmo, A. (2021). Tool for comparing mathematics tasks from paper-based and digital environments. *International Journal of Science and Mathematics Education, 19*, 1655–1675. https://doi.org/10.1007/s10763-020-10119-0

Lerman, S. (2000). The social turn in mathematics education research. In J. Boaler (Ed.), *Multiple perspectives on mathematics teaching and learning* (pp. 19–44). Ablex Publishing.

Liston, M., & O’Donoghue, J. (2009). Factors influencing the transition to university service mathematics: Part 1 a quantitative study. *Teaching Mathematics and Its Applications, 28*(2), 77–87. https://doi.org/10.1093/teamat/hrp006

Liston, M., & O’Donoghue, J. (2010). Factors influencing the transition to university service mathematics: Part 2 a qualitative study. *Teaching Mathematics and Its Applications, 29*(2), 53–68. https://doi.org/10.1093/teamat/hrp005

Lithner, J. (2011). University mathematics students’ learning difficulties. *Education Inquiry, 2*(2), 289–303. https://doi.org/10.3402/edui.v2i2.21981

Lyakhova, S., & Neate, A. (2019). Further mathematics, student choice and transition to university: Part 1 - Mathematics degrees. *Teaching Mathematics and Its Applications, 38*(4), 167–190. https://doi.org/10.1093/teamat/hry013

Maciejewski, W. (2018). Changes in attitudes revealed through students’ writing about mathematics. In E. Bergqvist, M. Österholm, C. Granberg, & L. Sumpter (Eds.), *Proceedings of the 42nd Conference of the international group for the psychology of mathematics education* (Vol. 3, pp. 339–346). PME.

Meehan, M., Howard, E., & Ní Shíleálaígháin, A. (2018). Students’ sense of belonging to mathematics in the secondary-tertiary transition. In E. Bergqvist, M. Österholm, C. Granberg, & L. Sumpter
Nihoul C. (2016). Quelques difficultés d’étudiants universitaires à reconnaître les objets « droites » et « plans » dans l’espace : Une étude de cas. In E. Nardi, C. Winslow & T. Hausberger (Eds.), Proceedings of the first conference of the international network for didactic research in university mathematics. University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/INDRUM2016/public/indrumbrief2016proceedings.pdf.

O’Shea, A., & Breen, S. (2021). Students’ views on transition to university: The role of mathematical tasks. Canadian Journal of Science, Mathematics and Technology Education, 21(1), 29–43. https://doi.org/10.1080/242330-021-00140-y

Ottinger, S., Kollar, I., & Ufer, S. (2016). Content and form — All the same or different qualities of mathematical arguments? In C. Csikos, A. Rausch, & J. Szitányi (Eds.), Proceedings of the 40th conference of the international group for the psychology of mathematics education (Vol. 4, pp. 19–26). PME.

Pampaka, M., Williams, J., & Hutcheson, G. (2012). Measuring students’ transition into university and its association with learning outcomes. British Educational Research Journal, 38(6), 1041–1071. https://doi.org/10.1080/01411926.2011.613453

Pan, M. L. (2016). Preparing literature reviews: Qualitative and quantitative approaches – fifth edition. Routledge. https://doi.org/10.4324/9781315265872

Pepin, B. (2014). Using the construct of the didactic contract to understand student transition into university mathematics education. Policy Futures in Education, 12(5), 646–657. https://doi.org/10.2304/pfie.2014.12.5.646

Pepin, B. (2014a). Student transition to university mathematics education: Transformations of people, tools and practices. In S. Rezat, M. Hattermann, A. Peter-Koop (Eds.), Transformation - A fundamental idea of mathematics education (pp. 65–83). Springer. https://doi.org/10.1007/978-1-4614-3489-4_4

Petropoulou, G., Jaworski, B., Potari, D., & Zachariades, T. (2016). Addressing large cohorts of first year mathematics students in lectures. In E. Nardi, C. Winslow & T. Hausberger (Eds.), Proceedings of the first conference of the international network for didactic research in university mathematics (pp. 390–399). Montpellier, France: University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01337916/document.

Pigge, C., Neumann, I., & Heinez, A. (2017). Which mathematical prerequisites do university teachers expect from STEM freshmen? In B. Kaur, W. K. Ho, T. L. Toh & B. H. Choy (Eds.), Proceedings of the 41st conference of the international group for the psychology of mathematics education (Vol. 4, pp. 25–32). PME.

Pustelnik, K., & Halverscheid, S. (2016). On the consolidation of declarative mathematical knowledge at the transition to tertiary education. In C. Csikos, A. Rausch, J. Szitányi (Eds.), Proceedings of the 40th conference of the international group for the psychology of mathematics education (Vol. 4, pp. 107–114). PME.

Quéré, P. V. (2016). Une étude de l’autonomie en mathématiques dans la transition secondaire-supérieur. In E. Nardi, C. Winslow & T. Hausberger (Eds.), Proceedings of the first conference of the international network for didactic research in university mathematics (pp. 484–493). University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01337937/document

Rabardel, P. (2002). People and technology: A cognitive approach to contemporary instruments. Université Paris 8. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/file/index/docid/1020705/filename/people_and_technology.pdf

Rach, S., & Heinez, A. (2011). Studying mathematics at university: The influence of learning strategies. In B. Ubuz (Ed.), Proceedings of the 35th conference of the international group for the psychology of mathematics education (Vol. 4, pp. 9–16). PME.

Rach, S., Ufer, S., & Kosiol, T. (2018). Situational interest in university mathematics courses: Similar for real-world problems, calculations, and proofs? In V. Durand-Guerrier, R. Hochmuth, S. Goodchild & N. M.
The transition from school to university in mathematics education…

Hogstad (Eds.), *Proceedings of the second conference of the international network for didactic research in university mathematics* (pp. 356–365). University of Agder and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01849960/document.

Rach, S., & Heinze, A. (2017). The transition from school to university in mathematics: Which influence do School-related variables have? *International Journal of Science and Mathematics Education, 15*(7), 1–21. https://doi.org/10.1007/s10763-016-9744-8

Rach, S., & Ufer, S. (2020). Which prior mathematical knowledge is necessary for study success in the university study entrance phase? Results on a new model of knowledge levels based on a reanalysis of data from existing studies. *International Journal of Research in Undergraduate Mathematics Education, 6*, 375–403. https://doi.org/10.1007/s40753-020-00112-x

Rach, S. (2021). Relations between individual interest, experiences in learning situations and situational interest. In M. Inprasitha, N. Changsri & N. Boonsena (Eds.), *Proceedings of the 44th conference of the international group for the psychology of mathematics education* (Vol. 3, pp. 491–500). PME.

Roos, A. (2019). Using grundvorstellungen and concept image theory for analysing and discussing students’ challenges in the transition from school to university — The example of extreme point. In M. Graven, H. Venkat, A. Essien & P. Vale (Eds.), *Proceedings of the 43rd conference of the international group for the psychology of mathematics education* (Vol. 3, pp. 265–272). PME.

Schäfer, I. (2013). Recognising different aspects as a key to understanding: A case study on linear maps at university level. In A. Lindmeier & A. Heinze (Eds.), *Proceedings of the 37th conference of the international group for the psychology of mathematics education* (Vol. 4, pp. 153–160). PME.

Schoenfeld, A. (2000). Purposes and methods of research in mathematics education. *Notices of the American Mathematical Society, 47*(6), 641–649.

Schüler-Meyer, A. (2019). How do students revisit school mathematics in modular arithmetic? Conditions and affordances of the transition to tertiary mathematics with a focus on learning Processes. *International Journal of Research in Undergraduate Mathematics Education, 5*, 163–182. https://doi.org/10.1007/s40753-019-0088-3

Selden, A. (2012). Transitions and proof and proving at tertiary level. In G. Hanna & M. de Villiers (Eds.), *Proof and proving in mathematics education. New ICMI study series* (pp. 391–420). Springer. https://doi.org/10.1007/978-94-007-2129-6_17

Sfard, A., & Prusak, A. (2005). Telling identities: In search of an analytic tool for investigating learning as a culturally shaped activity. *Educational Researcher, 34*(4), 14–22. https://doi.org/10.3102/0013189X034004014

Sfard, A. (2008). *Thinking as communicating. Human development, the growth of discourse, and mathematizing*. Cambridge University Press. https://doi.org/10.1017/CBO9780511499944

Sommerhoff, D., & Ufer, S. (2019). Acceptance criteria for validating mathematical proofs used by school students, university students, and mathematicians in the context of teaching. *ZDM-Mathematics Education, 51*, 717–730. https://doi.org/10.1007/s11858-019-01039-7

Tall, D. (1991). Advanced mathematical thinking. *Kluwer*. https://doi.org/10.1007/978-0-306-47203-1

Tall, D. (2008). The transition to formal thinking in mathematics. *Mathematics Education Research Journal, 20*, 5–24. https://doi.org/10.1007/BF03217474

Tall, D. (2013). How humans learn to think mathematically. *Cambridge University Press*. https://doi.org/10.1017/CBO9781139565202

Tall, D., & Vinner, S. (1981). Concept image and concept definition in mathematics with particular reference to limits and continuity. *Educational Studies in Mathematics, 12*(2), 151–169. https://doi.org/10.1007/BF00305619

Tall, D. (2004). Thinking through three worlds of mathematics. In M. Hoines, & A. Fuglestad (Eds.), *Proceedings of the 28th conference of the international group for the psychology of mathematics education* (Vol. 4, pp. 281–288). PME.

Thoma, A., & Nardi, E. (2018). Transition from school to university mathematics: Manifestations of unresolved commognitive conflict in first year students’ examination scripts. *International Journal of Research in Undergraduate Mathematics Education, 4*, 161–180. https://doi.org/10.1007/s40753-017-0064-3

Thomas, M., de Freitas Druck, I., Huillet, D., Ju, M., Nardi, E., Rasmussen, C., & Xie, J. (2015) Key mathematical concepts in the transition from secondary school to university. In S. Cho (Ed.), *Proceedings of the 12th international congress on mathematical education* (pp. 265–284). Springer. https://doi.org/10.1007/978-3-319-12688-3_18

Thomas, M., & Klymchuk, S. (2012). The school–tertiary interface in mathematics: Teaching style and assessment practice. *Mathematical Education Research Journal, 24*, 283–300. https://doi.org/10.1007/s13394-012-0051-6
Ufer, S., Rach, S., & Kosiol, T. (2017). Interest in mathematics = interest in mathematics? What general measures of interest reflect when the object of interest changes. *ZDM-Mathematics Education, 49*, 397–409. https://doi.org/10.1007/s11858-016-0828-2

Ufer, S. (2015). The role of study motives and learning activities for success in first semester mathematics studies. In K. Beswick, T. Muir & J. Fielding-Wells (Eds.) *Proceedings of the 39th conference of the international group for the psychology of mathematics education* (Vol. 4, pp. 265–272). PME.

Vandebrouck, F., & Leidwanger, S. (2016). Students’ visualization of functions from secondary to tertiary level. In E. Nardi, C. Winsløw & T. Hausberger (Eds.), *Proceedings of the first conference of the international network for didactic research in university mathematics* (pp. 153–162). University of Montpellier and INDRUM. Retrieved September 30, 2022, from https://hal.archives-ouvertes.fr/hal-01337928/document.

Varsavsky, C. (2012). Use of CAS in secondary school: A factor influencing the transition to university-level mathematics? *International Journal of Mathematical Education in Science and Technology, 43*(1), 33–42. https://doi.org/10.1080/0020739X.2011.582179

Vollstedt, M., Heinze, A., Gojdka, K., & Rach, S. (2014). Framework for examining the transformation of mathematics and mathematics learning in the transition from school to university. In S. Rezat, M. Hattermann, A. Peter-Koop, (Eds.) *Transformation - A fundamental idea of mathematics education* (pp. 29–50). Springer. https://doi.org/10.1007/978-1-4614-3489-4_2

Wenger, E. (1998). Communities of practice: Learning, meaning and identity. *Cambridge University Press*. https://doi.org/10.1017/CBO9780511803932

Winsløw, C. (2008). Transformer la théorie en tâches: La transition du concret à l’abstrait en analyse réelle. In A. Rouchier & I. Bloch (Eds.) *Actes de la XIIIème école d’été en didactique des mathématiques*. La Pensée Sauvage.

**Publisher’s note** Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

**Authors and Affiliations**

Pietro Di Martino¹ · Francesca Gregorio²³ · Paola Iannone⁴

Francesca Gregorio
francesca.gregorio@hepl.ch

Paola Iannone
p.iannone@lboro.ac.uk

¹ Department of Mathematics, Università Di Pisa, Largo B. Pontecorvo 5, 56125 Pisa, Italy

² Université de Paris, Univ. Paris Est Creteil, CY Cergy Paris Université, Univ. Lille, UNIROUEN, LDAR, F-75013 Paris, France

³ Haute École Pédagogique du Canton de Vaud, Lausanne, Switzerland

⁴ Department of Mathematics Education, Loughborough University, Loughborough LE11 3TU, UK