Laser cooling scheme for the carbon dimer (^{12}C_2)

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We report on a scheme for laser cooling of ^{12}C_2. We have calculated the branching ratios for cycling and repumping transitions and calculated the number of photon scatterings required to achieve deflection and laser cooling of a beam of C_2 molecules under realistic experimental conditions. Our results demonstrate that C_2 cooling using the Swan (d^3\Pi_\sigma \leftrightarrow a^3\Pi_u) and so-called Duck (d^3\Pi_\sigma \leftrightarrow c^3\Sigma_u^+) bands is achievable via techniques similar to state-of-the-art molecular cooling experiments. The Phillips (A^1\Pi_u \leftrightarrow X^1\Sigma_g^+) and Ballik-Ramsay (b^3\Sigma_- \leftrightarrow a^3\Pi_u) bands offer the potential for narrow-line cooling. This work opens up a path to cooling of molecules with carbon-carbon bonds and may pave the way toward quantum control of organic molecules.

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Ultracold molecules offer exciting prospects for quantum sensing [1–3], quantum chemistry [4,5], quantum simulation [6–12], and quantum computing [13–15]. To pursue such applications, laser cooling of molecules [16] has been successfully demonstrated over recent years, utilizing molecules with quasidiagonal Franck-Condon factors, such as SrF [17,18], CaF [19–21], YbF [22], BaH [23], CaOH [24], CaOCH_3 [25], Yo [26], SrOH [27], and YbOH [28]. These molecules are suitable for laser cooling, but their applications beyond fundamental physics are limited. A parallel approach to laser cooling, namely optoelectric Sisyphus cooling, has been used to slow down molecules such as CH_3F [29] and H_2CO [30], but it is limited to dipolar molecules. Extending laser cooling and quantum control to molecules with significant off-diagonal Franck-Condon factors, including molecules that play a broader role in chemistry, promises to open up intriguing research frontiers.

Molecules and compounds containing carbon atoms are of paramount importance across science. Networks of carbon atoms, such as graphene [31,32], carbon nanotubes [33], and fullerences [34,35], have unique electronic, optical, and mechanical properties. Molecules involving carbon-carbon and carbon-hydrogen bonds are fundamental to organic chemistry. Carbon-bearing molecules and compounds are also observed in astrophysical environments [36] and play an important role in planet formation and astrobiology [37]. Quantum control of carbon-bearing molecules would offer the opportunity to prepare isotopically pure molecular samples and provide a new tool set for precision studies of these molecules.

Here, we develop a laser cooling scheme for the carbon dimer (C_2). C_2 is the minimal instance of a carbon chain and a building block of organic molecules. The C-C bond is relevant in alkynes, alkenes, and aromatics [38]; C_2 is used as a center for the nucleation of carbon nanotubes [39]; and it has been observed in interstellar space [40]. Laser cooling on the C-C bond may enable laser cooling of more complex molecules with a similar bond.

Direct optical control of atomic carbon is extremely challenging, as any relevant cooling transitions lie deep in the ultraviolet range that is difficult to access experimentally [41,42]. In contrast, relevant electronic transitions of carbon dimers lie in the visible and infrared ranges that are more readily accessible.

The carbon dimer has several features that are favorable for a laser cooling scheme: (i) The low-energy electronic structure features only singlet and triplet states similar to group 2 atoms and bialkali molecules. (ii) The rovibrational spectrum is sparse due to relatively large vibrational and rotational spacings of about 1500 and 1.5 cm^{-1}, respectively, which limits the number of possible decay paths. This is a result of the small mass of carbon atoms and the tight bond between them (Fig. 1). (iii) ^{12}C, the most abundant carbon isotope with a relative abundance of 98.9% [43], has no nuclear spin (I = 0). Therefore, the ^{12}C dimer does not have a hyperfine structure. This is a remarkable simplification over the general case where a complex hyperfine structure can lead to dark states and inhibit efficient photon cycling. (iv) The homonuclear nature of C_2 reduces the number of allowed transitions due to selection rules arising from the nuclear exchange symmetry [44]. (v) The energy scale of spin-orbit coupling (with coupling constants on the order of 10 cm^{-1} [45]) is smaller than the typical spacings between vibrational levels. Hence, population loss into the opposite spin manifold during laser cooling is expected to be small [45].

We analyze three laser cooling schemes. We evaluate them in terms of photon-cycling closure and calculate the achievable light forces. Specifically, we consider four transition bands between the six lowest-lying electronic states of C_2 (Fig. 1). These are the Phillips (A^1\Pi_u \leftrightarrow X^1\Sigma_g^+), the Ballik-Ramsay (b^3\Sigma_- \leftrightarrow a^3\Pi_u), the Swan (d^3\Pi_\sigma \leftrightarrow a^3\Pi_u), and
so-called Duck (d$^3\Pi_g \leftrightarrow c^3\Sigma^+_g$) bands.\(^1\) Other transition bands between these electronic states do not exist due to selection rules, as detailed below. We find that the Swan and Duck bands together offer a promising pathway for laser cooling of a C\(_2\) beam. Due to small scattering rates, the Phillips and Ballik-Ramsay bands only provide weak optical forces, but they may be suitable for narrow-line cooling, similar to laser cooling schemes for alkaline earth atoms [47–49].

For our analysis, we use existing spectroscopic data. The spectrum of C\(_2\) has been extensively studied [45,50] to facilitate its identification in astrophysical environments [51,52], to understand its photodissociation in comets [53], to determine thermodynamic functions relevant to astrochemical reactions [54], and to benchmark quantum chemistry calculations [55]. Our main data source is the ExoMol Project [56–59], which uses a combination of first-principles theoretical calculations and experimental data. From these data, we extract transition frequencies and Einstein coefficients, from which we calculate branching ratios (BR) of possible decay paths [60]. The branching ratios and scattering rates fully characterize the decay paths of spontaneous emission and the molecule-light interaction; a separate evaluation of Franck-Condon factors is not needed. An overview of the vibrational levels relevant to this study is shown in Fig. 2.

We first discuss the starting conditions for the three cycling schemes under consideration. For the Phillips band, we start in the absolute ground state, X$^1\Sigma^+_g \left[ v, J \right] = \{ 0, 0 \}$, and we excite to the A$^3\Pi_{1u} \left[ 0, 1 \right]$ state. Here, \( v \) is the vibrational quantum number and \( J \) is the total angular momentum. The subscripts 0 and 1 indicate the \( \Omega \) quantum number, which is the projection of the total electronic angular momentum onto the internuclear axis [61]. From the excited state, population decays into vibrational states of X$^1\Sigma^+_g \left[ J = 0 \right]$ and 2. The relevant branching ratios are shown in Fig. 3(a), calculated using the Einstein coefficients \( A_i \) for spontaneous decay to a state \( i \) [57]. Branching ratios are given by BR\(_i = A_i / \sum_j A_j \). where the sum runs over all possible decay paths. The splittings between the \( J = 0 \) and 2 states are about 10 cm\(^{-1} \approx h \times 300 \) GHz (where \( h \) is Planck’s constant). While decays to \( b^3\Sigma^-_g \) are spin-forbidden, they happen with BR\(_i < 10^{-9} \) and are therefore irrelevant for our study. Decays to \( a^3\Pi_u \) are not observed, as they are spin-forbidden, reflection-symmetry-forbidden, and they do not fulfill the \( gerade \leftrightarrow ungerade \) selection rule.

For the Ballik-Ramsay band, we start from the \( a^3\Pi_{1u} \left[ 0, 1 \right] \) state and excite to the \( b^3\Sigma^+_g \left[ 0, 0 \right] \) state. Excitation from \( J = 1 \) to 0 is advantageous, reducing the number of possible decay paths. The relevant BR’s are shown in Fig. 3(b). Only decays back into \( J = 1 \) states of \( a^3\Pi_u \) are relevant, while decays to \( X^1\Sigma^+_g \) are spin-forbidden and strongly suppressed [62]. The \( J = 1 \) states comprise \( \Omega = 0 \) and 1 states that split by about 17 cm\(^{-1} \approx h \times 500 \) GHz.

For the Swan and Duck scheme, we start in the metastable triplet vibrational ground state \( a^3\Pi_{1u} \left[ 0, 1 \right] \) and excite to the \( d^3\Pi_{g} \left[ 0, 0 \right] \) state. Transitions between \( d^3\Pi_{g} \left[ 0, 0 \right] \) and \( a^3\Pi_{u} \left[ 0, 0 \right] \) are strongly suppressed as \( J = 0 \rightarrow 0 \) transitions are forbidden [61]. The relevant BR’s for decay into \( c^3\Sigma^+_u \) and \( a^3\Pi_u \) are shown in Fig. 3(c). The doublets for decay into \( c^3\Sigma^+_u \) have identical \( v \) and \( J \) and differing \( \Omega \), similar to the Ballik-Ramsay band. Decay from \( d^3\Pi_{g} \rightarrow a^3\Pi_{1u} \) is not fully suppressed but extremely weak (BR\(_i < 10^{-6} \)) due to the small singlet-triplet mixing, and it can be neglected here. Decay from \( c^3\Sigma^+_u \) to \( b^3\Sigma^+_g \) is suppressed as radiative transitions cannot change the \( +/− \) symmetry of \( \Sigma \) states [61]. Transitions from \( c^3\Sigma^+_u \rightarrow a^3\Pi_{1u} \) are not allowed due to the \( gerade \leftrightarrow ungerade \) selection rule [61]. Forbidden decays to \( A^1\Pi_u \) due to spin-orbit coupling have BR\(_i < 10^{-7} \) and are therefore irrelevant to our study.

For each cycling scheme, we determine how many photons can be scattered, while retaining at least 10% of the initial molecular sample in bright states [60,63]. This serves as a metric for the cycling efficiency. By driving additional repumping transitions, the closure of the cycling

\footnote{Following the nomenclature of [46].}
schemes is improved, enabling a larger number of scatterings before reaching the 10%-retention metric. We model photon scattering as a Bernoulli process with a probability \( p \) that the molecule will remain within the cycling scheme per photon scattering \([63]\), and a probability \( 1 - p \) that the molecule will leave. As such, \( p \) is a measure of closure for a photon cycling scheme. It depends on the number of driven transitions and is given by \( p = \sum_{i} \text{BR}_i \), where \( i \) runs over all driven transitions. Figure 3 shows the BR’s of the relevant decay paths out of the excited state of each cycling scheme. The fraction of molecules in bright states after \( n \) cycles is given by \( p^n \). The number of scatterings that retain 10% of the molecules in a bright state is \( n_{10\%} = \ln(0.1) / \ln(p) \).

For each scheme, we also determine how long it will take for a certain number of photon scatterings to happen. Combined with the initial velocity of the molecules, this determines whether cooling can be achieved within the spatial dimensions of a practical experimental setup. The time for \( n_{10\%} \) scatterings is given by \( t_{10\%} = n_{10\%} / R \), where \( R = \Gamma / (G + 1 + 2 \sum_{i} I_{\text{sat},i} / I_i) \) is the scattering rate \([16,60,64]\). Here \( \Gamma \) is the excited state linewidth; \( I_i \) is the intensity of the laser addressing the \( i \)th transition, set to \( I_i = 10^3 \, \text{mW cm}^{-2} \); \( I_{\text{sat},i} = \pi h c \Gamma / 3 \lambda_i^3 \) is the associated saturation intensity \([16]\); and \( G \) is the number of driven transitions. In the definition of saturation intensity, \( c \) is the speed of light and \( \lambda_i \) the wavelength of the addressed transition. Saturation intensities are \( \lesssim 1.5 \, \text{mW cm}^{-2} \) for the Swan and Duck bands, \( \lesssim 1 \, \mu \text{W cm}^{-2} \) for the Phillips band and \( \lesssim 0.2 \, \mu \text{W cm}^{-2} \) for the Ballik-Ramsay band.

We calculate \( n_{10\%} \) and \( t_{10\%} \) for all three schemes. The results in Table I show that strong closure (\( p > 0.999 \)) can be reached by addressing eight transitions in the Phillips scheme, six transitions in the Ballik-Ramsay scheme, and nine transitions in the Swan and Duck scheme. However, the time to complete a few thousand scattering processes varies from about 1 s for the Phillips and Ballik-Ramsay schemes to a few milliseconds for the Swan and Duck scheme.

To assess the practical implications of this analysis, we consider two specific cases of molecule-light interactions for a molecular beam of \( \text{C}_2 \), illustrated in Fig. 4: (i) transverse deflection and (ii) longitudinal cooling. Deflection is a useful technique to isolate \( \text{C}_2 \) from a multispecies carbon beam for the preparation of pure samples. Longitudinal cooling can bring molecules to a near-standstill. For the initial molecular beam, we assume that \( \text{C}_2 \) emerges from a cryogenic buffer gas source with a translational temperature of 4 K, similar to current experiments on laser cooling of molecules \([17,20,22,23,65,66]\). At this temperature, the thermal forward velocity of \( \text{C}_2 \) is on the order of \( v = 100 \, \text{m s}^{-1} \). We note, however, that velocities as low as \( v = 60 \, \text{m s}^{-1} \) should be achievable in an optimized flow regime.

For transverse deflection, we assume that the lasers impinge perpendicularly on the molecular beam [Fig. 4(a)]. As photons are scattered, the associated recoil velocity leads to an
TABLE I. Closure, number of scatterings, and scattering time for an increasing number of driven transitions in the Swan and Duck (S and D), Phillips (P), and Ballik-Ramsay (B) schemes.

| Driven transitions | $p$     | $n_{10\%}$ | $t_{10\%}$ (ms) |
|--------------------|---------|-------------|-----------------|
| Swan and Duck      |         |             |                 |
| S1                 | 0.75638 | 8           | 0.002           |
| S1-S2              | 0.91873 | 27          | 0.01            |
| S1-S3              | 0.95440 | 49          | 0.02            |
| S1-S4              | 0.97646 | 96          | 0.06            |
| S1-S4, D1          | 0.98573 | 160         | 0.1             |
| S1-S5, D1          | 0.99324 | 339         | 0.3             |
| S1-S5, D1-D2       | 0.99596 | 568         | 0.5             |
| S1-S6, D1-D2       | 0.99836 | 1406        | 1.5             |
| S1-S7, D1-D2       | 0.99936 | 3621        | 4.2             |
| Phillips           |         |             |                 |
| P1                 | 0.45290 | 2           | 0.1             |
| P1-P2              | 0.67861 | 5           | 0.2             |
| P1-P3              | 0.86793 | 16          | 0.8             |
| P1-P4              | 0.96210 | 59          | 3.9             |
| P1-P5              | 0.98650 | 169         | 13              |
| P1-P6              | 0.99860 | 1639        | 151             |
| P1-P7              | 0.99953 | 4925        | 517             |
| P1-P8              | 0.99990 | 407409      | 48140           |
| Ballik-Ramsay      |         |             |                 |
| B1                 | 0.78944 | 9           | 0.3             |
| B1-B2              | 0.94837 | 43          | 2.3             |
| B1-B3              | 0.98539 | 156         | 11              |
| B1-B4              | 0.99266 | 312         | 28              |
| B1-B5              | 0.99966 | 6788        | 738             |
| B1-B6              | 0.99997 | 80585       | 10224           |

TABLE II. Results of the photon scattering analysis for transverse deflection and longitudinal cooling.

| Driven transitions | $n_{\text{eff}}$ | $L_{\text{defl}}$ (m) | $\vartheta$ (deg) | Driven transitions |
|--------------------|------------------|-----------------------|-------------------|-------------------|
| Swan and Duck      |                  |                       |                   |                   |
| S1-S7, D1-D2       | 338              | 0.02                  | 6.1               | S1-S5, D1         |
| Phillips           |                  |                       |                   |                   |
| P1-P7              | 611              | 5.6                   | 4.4               | P1-P6             |
| Ballik-Ramsay      |                  |                       |                   |                   |
| B1-B5              | 1941             | 21                    | 9.8               | B1-B5             |

For longitudinal cooling, we assume that the laser beams counterpropagate to the molecular beam [Fig. 4(b)]. We also assume that the Doppler shift arising in the course of slowing is compensated by an appropriate technique, such as a counteracting Zeeman shift [67] or chirped laser frequencies [19]. The number of scatterings necessary to reach rest, $n_{\text{cool}}$, is obtained by dividing the molecule’s initial momentum by that of an average photon [63]. We calculate the expected distance over which the beam is slowed to a near-standstill, $L_{\text{cool}}$, and the time to fully slow the beam, $t_{\text{cool}}$ [60].

The results for deflection and cooling are shown in Table II. The Swan and Duck scheme is favorable with a deflection angle of $\vartheta \sim 6^\circ$ achieved by illuminating the molecules with S1-S5 and D1 (labeled as in Fig. 3) over $L_{\text{defl}} \sim 2$ cm of axial travel, an experimentally feasible laser beam size. Cooling to a near-standstill is viable by addressing S1-S7 and D1-D2 over $L_{\text{cool}} \sim 16$ cm. The deceleration due to the light force is about $3 \times 10^4$ m s$^{-2}$, and cooling to the Doppler temperature is achieved within $3$ ms of the molecules leaving the source. The scattering rate is $R \sim 1$ MHz. During cooling, about $3.2 \times 10^3$ photons are scattered per molecule, which corresponds to the BR cutoff of $3 \times 10^{-4}$ indicated in Fig. 3. Due to the narrow linewidth of the Phillips and Ballik-Ramsay bands (scattering rates of $R \sim 9$ kHz), extremely long and thus impractical interaction regions are needed in a deflection experiment. Longitudinal cooling on these two bands is similarly impractical due to the small deceleration of $\sim 100$ m s$^{-2}$ that would require a beam line of $L_{\text{cool}} \geq 10$ m to reach standstill. Therefore, the Phillips and Ballik-Ramsay schemes are not suitable for longitudinal slowing or direct capture in a magneto-optical trap. However, they may be useful for narrow-line cooling to reach lower Doppler temperatures in a magneto-optical trap after initial laser cooling.

Based on our findings, laser cooling of C$_2$ is conceptually feasible. Also, it should be experimentally feasible using currently available technology. Figure 5(a) shows the transition wavelengths for the Swan and Duck scheme. Laser light for all transitions can be generated with diode lasers, either directly or after frequency doubling. Diodes for 516 (S1 and S3), 685 (S6), 932 (D1), and 1150 nm (D2) are readily available. Light at 563 (S2 and S5) and 618–619 nm (S4 and S7) can be generated via frequency doubling of laser diodes. The Phillips and

an increasing Doppler shift that detunes the molecules out of resonance with the cooling lasers. This determines the achievable deflection angle $\vartheta$ [see Fig. 4(a)]. Further photon scattering is suppressed when the Doppler shift equals the linewidth $\delta = \Gamma / 2\sqrt{1+I/I_{\text{sat}}}$. For simplicity, we only take into account scattering from the main transition here and assume $I = 10^3$ mW cm$^{-2}$. The number of scatterings $n_{\text{eff}}$ at which the Doppler detuning suppresses further photon scattering is found by dividing the initial momentum of a molecule by that of an average photon [60]. Using $R$, we calculate the time necessary to complete $n_{\text{eff}}$ scatterings and the distance traveled by molecules in the axial direction, $L_{\text{defl}}$. From the calculated transverse velocity, $v_\perp$, and the axial velocity, $v = 100$ m s$^{-1}$, we obtain $\vartheta$.

(a) Buffer gas source $v = 100$ m/s $\theta$ $\vartheta = 6^\circ$

(b) Buffer gas source $v = 100$ m/s $L_{\text{defl}}$ $v = 0$ m/s $L_{\text{cool}}$ Cooling lasers $v = 0$ m/s $\vartheta = 6^\circ$

FIG. 4. Schematic of C$_2$ experiments for (a) beam deflection and (b) longitudinal cooling.
Ballik-Ramsay schemes are more challenging, as the infrared frequencies shown in Figs. 5(b) and 5(c) are currently harder to generate at the required power levels.

In addition to the lasers, a cryogenic source for the generation of a cold beam of carbon beam is needed. The basic technology of cryogenic buffer gas cooling has been developed and refined over the past two decades [66,68]. Hot carbon vapor to seed the buffer gas cell can be created via ablation of a graphite target [69,70] or evaporation of graphite rods via resistive heating [71]. These have been shown to generate vapor containing mixtures of various carbon compounds, including C, C2, Cn, fullerenes, etc., whose exact ratios can be controlled by varying experimental parameters. For example, ablation sources can produce carbon beams with a typical composition of $\sim 10\%$ of C2 [69], and it has been shown that beam shaping of the ablation pulse can further enhance the formation of C2 [70]. In the ablation process, a significant C2 fraction is found to be produced in the triplet states of $^3\Pi_u$ [70,72]. Assuming an initial temperature of $\sim 5000$ K, the population in the triplet ground state is about 80% of the singlet ground state [73]. The relaxation of electron spin and the rotational degrees of freedom have a cross section that is about 100 times smaller than translational thermalization [66,68,74,75]. The density and in-cell time prior to extraction can be tuned such that a significant fraction of population will be available in the $^3\Pi_u |0, 1\rangle$ state for the Swan and Duck cooling scheme. Extended lifetimes in triplet electronic states of molecules with a singlet ground state have been experimentally observed previously in a buffer gas cell [76].

In conclusion, we have laid out a laser cooling scheme for C2 that is experimentally feasible using state-of-the-art technology. The scheme differs from the current paradigm of laser cooling of molecules with highly diagonal Franck-Condon factors, showing that laser cooling can be possible despite significant off-diagonal Franck-Condon factors. This work lays the foundation for future studies, such as a concept for a magneto-optical trap [77] to enable the creation of ultracold ensembles of C2 molecules, and possibly the trapping of individual C2 molecules in optical tweezer traps [78]. The narrow lines in the Phillips and Ballik-Ramsay bands may be useful for coherent cooling schemes, such as bichromatic and polychromatic cooling [79–82]. The energy levels and transitions identified in this work may further guide the development of a Zeeman-Sisyphus cooling scheme [83]. More generally, our findings open up paths towards precision spectroscopy of C2 in laser-cooled samples, towards laser cooling of carbon chains, and may constitute a first step towards quantum control of organic molecules.

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