Single-shot Embedding Dimension Search in Recommender System

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ABSTRACT
As a crucial component of most modern deep recommender systems, feature embedding maps high-dimensional sparse user/item features into low-dimensional dense embeddings. However, these embeddings are usually assigned a unified dimension, which suffers from the following issues: (1) high memory usage and computation cost. (2) sub-optimal performance due to inferior dimension assignments. In order to alleviate the above issues, some works focus on automated embedding dimension search by formulating it as hyper-parameter optimization or embedding pruning problems. However, they either require well-designed search space for hyperparameters or need time-consuming optimization procedures. In this paper, we propose a Single-Shot Embedding Dimension Search method, called SSEDS, which can efficiently assign dimensions for each feature field via a single-shot embedding pruning operation while maintaining the recommendation accuracy of the model. Specifically, it introduces a criterion for identifying the importance of each embedding dimension for each feature field. As a result, SSEDS could automatically obtain mixed-dimensional embeddings by explicitly reducing redundant embedding dimensions based on the corresponding dimension importance ranking and the predefined parameter budget. Furthermore, the proposed SSEDS is model-agnostic, meaning that it could be integrated into different base recommendation models. The extensive offline experiments are conducted on two widely used public datasets for CTR (Click Through Rate) prediction task, and the results demonstrate that SSEDS can still achieve strong recommendation performance even if it has reduced 90% parameters. Moreover, SSEDS has also been deployed on the WeChat Subscription platform for practical recommendation services. The 7-day online A/B test results show that SSEDS can significantly improve the performance of the online recommendation model while reducing resource consumption.

CCS CONCEPTS
- Information systems → Recommender systems.

KEYWORDS
embedding dimension search, embedding pruning, recommender system, sparse learning

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1 INTRODUCTION
Recommender systems have been widely deployed to various scenarios such as advertisement [37], online shopping [3], news apps [35], and many others [1, 2, 21, 27, 30, 32]. The typical inputs of recommender systems are a large number of categorical (e.g., gender) or numerical (e.g., age) features associated with users and items. For example, in WeChat and Youtube platforms, more than a billion unique user ID features are encoded as high-dimensional sparse one-hot feature vectors. To well extract users’ preferences for personalized recommendations, most state-of-the-art recommendation methods, such as deep neural network (DNN) based methods [3, 4], factorization machine (FM) based methods [9, 17, 24, 28], map these high-dimensional sparse feature vectors into low-dimensional dense embeddings. Then these embeddings are utilized for further feature operations (e.g., feature interactions) to make final predictions. However, most of these methods set a fixed embedding dimension for all features, which could suffer from the following issues: (1) The embeddings could contain tens of billions of parameters
resulting in high memory usage and computation cost. (2) Over-parameterizing the low-frequency features might induce overfitting and even unexpected noise. On the other hand, high-frequency features need more parameters to convey fruitful information.

Nevertheless, manually setting appropriate embedding dimensions for different features is intractable due to the vast amount of candidate solutions. Thus, it is natural to think about how to assign embedding dimensions to different features in an automated manner, which is termed as embedding dimensions search (EDS) problem in this paper.

The early work [8] tries to address EDS by introducing a human-designed rule which assigns embedding dimensions according to the popularity of features. Recently, inspired by the success of neural architecture search (NAS) [39], some works employ NAS-based methods to handle EDS by formulating it as a hyper-parameter optimization (HPO) problem [36]. For example, NIS [10] and ESPN [19] search embedding dimensions from a set of predefined candidate dimensions by policy networks. DNIS [11] and AutoEmb [34] utilize the differential architecture search (DARTS) [18] method to enforce the search efficiency. However, this kind of method generally requires a well-designed search space for candidate embedding dimensions and expensive optimization processes to train the candidates. As an alternative solution to the EDS problem, some works [5, 20, 29] treat EDS as an embedding pruning problem, eliminating requirements for predefining search space. Instead, they obtain the mixed-dimensional embeddings by identifying and removing the redundant embedding dimensions via additional mask layers with learnable threshold parameters. However, the embedding pruning based EDS methods need alternatively optimize threshold parameters and parameters of the model itself, which is time-consuming, thereby undermining their utility in practical recommendation services.

To alleviate the limitations mentioned above of embedding pruning based EDS methods, this paper needs to address the following challenges: a) **How to identify embedding dimensions for various feature fields?** The EDS problem could be transformed into identifying the importance of each dimension of embeddings. In this way, we could prune those relatively unimportant dimensions of embeddings such that the mixed dimension embeddings are automatically obtained. To this end, inspired by the weights pruning method [15] in DNN, we address this challenge in a data-driven manner, which introduces a criterion that could identify the importance (called saliency score) of each embedding dimension for each feature field based on its influence on the loss function. Specifically, we mask each embedding dimension of each feature field while keeping the others unchanged. Then we could compute the saliency scores of each dimension by measuring its influence on the loss function. b) **How to search embedding dimensions in an efficient way?** Based on the above idea, once we obtained the saliency scores, we could rank the embedding dimensions over all feature fields in descending order and retain a limited portion based on the given parameter budget. However, it is prohibitively expensive to identify the importance of each dimension one by one. Thus, we utilize an approximation operation [14] to efficiently measure the importance of all dimensions only in one forward-backward pass, namely single-shot embedding pruning. Hence, one significant advantage of SSEDS is its efficiency, which makes it suitable for practical industry recommender systems requiring frequently (e.g., per hour) updating models due to the real-time changes in feature distribution. c) **How to integrate the proposed SSEDS into traditional recommendation models?** The traditional recommendation models, especially FM based methods [9, 17, 24, 28], utilize explicit feature interaction operations (e.g., the dot product) to capture cross feature relations, requiring all embeddings to have the same dimension. To make the proposed SSEDS be seamlessly integrated into various traditional models, we propose first to pre-train the traditional model in a standard way, and then obtain a slim model with mixed-dimensional embeddings via the proposed single-shot embedding pruning. Finally, we initialize and retrain the slim model using the pretrained and mixed-dimensional embeddings, and introduce additional transform matrices for each feature field to align dimensions for further feature interaction operations.

In summary, the main contributions of this paper are as below:

- This paper proposes an effective and efficient single-shot embedding dimension search method, called SSEDS, which introduces a criterion that could identify the importance of each embedding dimension of each field only in one forward-backward pass. In this way, the mixed-dimensional embeddings are efficiently obtained.
- The proposed SSEDS is model-agnostic. It proposes to utilize linear transform matrices to align the various dimensions for different feature fields such that SSEDS could be seamlessly integrated into various base recommendation models. On the other hand, it can flexibly control the number of pruned parameters to satisfy different requirements on the parameter budget.
- The extensive offline experiments are conducted on two public datasets for the CTR prediction task, and the experimental results demonstrate that SSEDS can still achieve strong recommendation performance even if it has reduced 90% parameters. Furthermore, SSEDS has also been deployed on the WeChat Subscription platform for practical recommendation service, and the 7-day online A/B test results show that SSEDS can significantly improve the performance of the online recommendation model while reducing resource consumption.

The rest of this paper is organized as follows. Section 2 reviews the main related work. Section 3 formulates the problem and details the proposed SSEDS. Section 4 introduces experimental settings and discusses experimental results, followed by a conclusion in Section 5.

## 2 RELATED WORK

This section introduces the main related works to our study, including feature-based recommendation models, embedding dimension search methods, and network pruning methods.

### 2.1 Feature-based Recommender System

The feature-based recommender system takes the high-dimensional and sparse features from user and item as inputs and maps them into a low-dimensional dense embedding space to better capture users’ preference for personalized recommendations. To generate effective representations, deep models are widely used and provide
state-of-the-art results [31]. The related works are flourishing. The linear regression (LR) model gets extensive applications in the early stage, which directly maps the raw features to continuous predictions via a single fully-connected layer. Then Wide&Deep [3] introduces an extra MLP branch for supplementing the high-level representation. Furthermore, DeepFM [9], and XDeepFM [17] turn eyes on modeling the concurrence of different features and propose factorization machine (FM). Recently, more complex deep neural layers are adopted in recommendation system, e.g., attention-based models such as AFN [4], AutoInt [25] and InterHAt [16]. However, these methods assign a fixed embedding dimension for all features regardless of their heterogeneity, which could downgrade the model performance and consume huge amount of storage and computing resources.

2.2 Embedding Dimension Search Methods
Studied on the EDS problem could be categorized into heuristic methods, hyper-parameter optimization (HPO) methods, and embedding pruning methods. The heuristic method such as MDE [8] allocates the embedding dimensions based on the popularity of features. However, using such simple rules to determine the embedding dimension suffers a loss of generality for various recommendation tasks.

Recently, inspired by the success of neural architecture search (NAS) [6, 39], some works model the EDS problem as HPO problems which automatically search embedding dimensions from a predefined candidate dimension set. For example, NIS [10] is the first work to formulate the EDS as an HPO problem, which optimizes the assignment for embedding dimensions by constantly improving the policy network with high cost on training time. Differently, some research work [11, 19, 33, 34] propose to use the differentiable architecture search (DARTS) [18] to enforce the search efficiency. For example, DNIS [11] adopts a soft layer to control the significance of each embedding dimension and prunes the unimportant components after training. AutoDim [33] utilizes a soft and continuous manner to calculate the weights over various dimensions for feature fields, then the embedding architecture is derived from the maximum weight. Besides, ESAPN [19] and AutoEmb [34] dynamically update the embedding structure for users and items regarding the on-time frequency as an important reference. However, HPO based EDS methods generally require well-designed search space for candidate embeddings and need iterative optimization procedures throughout training, thereby undermining their utility in practical recommendation services requiring high efficiency.

2.3 Network Pruning
Differently, instead of requiring predefined search space, embedding pruning based EDS methods selectively remove redundant embedding dimensions by introducing additional mask layers with learnable threshold parameters. For example, PEP [20] designs an adaptive threshold to filter out the redundant embedding dimensions with low magnitude, and ATML [29] calibrates the breaking point to identify the promising elements. Deeplight [5] proposes to prune both parameters in the embedding layer and DNN layer to solve the high-latency issues in CTR prediction. However, these methods either fail to reach high efficiency [5, 20, 29] due to the iterative optimization procedures or cannot strictly constrain the sparsity level [20, 29] required by various infrastructures.

3 PROPOSED METHOD
This section will first give a problem formulation of the embedding pruning based EDS under the given parameter budget for the feature-based recommender system1 and then elaborate on the proposed SSEDS.

3.1 Problem Formulation
The typical training data \(\mathcal{D}\) of the feature-based recommender system is commonly constructed from the users’ click records, and each record \((x, y)\) in \(\mathcal{D}\) is denoted as:

\[
(x, y) = ([x_1, x_2, \ldots, x_m], y)
\]

where \(x = \{x_1, x_2, \ldots, x_m\}\) is the raw feature vector that concatenates \(m\) feature fields associated with users and items, and \(y\) is the binary label (e.g., 1 for click and 0 for not click) describing the user’s preference for the given item. For each feature field (e.g., occupation), it contains a certain number of unique features (e.g., teacher, doctor and so on), thus the feature vector \(x_i \in x\) of the \(i\)-th field is usually encoded as the high-dimensional sparse one-hot or multi-hot vector. To well extract the user’s preference, most modern feature-based recommender systems map \(x_i \in \mathbb{R}^{n_i}\) (\(n_i\) is the number of unique features in field \(i\)) into a low-dimensional dense embedding \(e_i\) as follows:

\[
e_i = V_i x_i
\]

where \(V_i \in \mathbb{R}^{d \times n_i}\) is the embedding table of the \(i\)-th feature field, and \(d\) is the embedding dimension shared by all fields. The whole embedding table \(V = \{V_1, V_2, \ldots, V_m\}\) could be obtained by concatenating all the embedding table from each field.

Thus, the goal of a feature-based recommender system \(f\) is to predict the probability \(p\) about whether the user would click on the item as follows:

\[
p = f(x|V, \Theta)
\]

where \(\Theta\) represents other parameters of the model (e.g., parameters in deep layers of the Wide&Deep [3] and DeepFM [9]).

Finally, in order to obtain mixed-dimensional embeddings, the embedding pruning based EDS methods aim to identify and remove a certain number of embedding dimensions from the whole embedding table \(V\) based on the parameter budget \(k \in (0, 1]\) while minimizing the loss function as follows:

\[
V^*, \Theta^* = \arg\min_{V, \Theta} \mathcal{L}(\Theta, V; D), \ s.t. \ ||V^*||_0 < k||V||_0
\]

where \(\mathcal{L}\) is the loss function (e.g., cross-entropy), and \(|| \cdot ||_0\) represents the L0 norm, i.e., the desired non-zero parameters in final optimized pruned embedding table \(V^*\).

It is worth noting that the pruning under the recommender system scenario is different from the traditional network pruning methods introduced in Section 2.3. The main difference is that our method focuses on pruning embedding table \(V\) as it dominates the vast majority of parameters of the model, instead of the model parameters \(\Theta\) focused by traditional network pruning methods.

1We focus on the CTR prediction task in this paper.
Nevertheless, it is easy to extend our method to pruning both embedding table and model parameters.

3.2 SSEDS

Figure 1 displays the overview of the proposed SSEDS that contains three stages: pretraining, single-shot pruning, and retraining. Concretely, in the pretraining stage, we pretrain those traditional recommendation models with uniform-dimensional and over-parameterized embeddings in a standard manner to make these embeddings expressive. In the single-shot pruning stage, we first compute the saliency scores (more on this later) for each embedding dimension for each field based on its influence on the loss function, and then the saliency scores are ranked in descending order. Thus we can sequentially remove dimensions with low saliency scores until the parameter budget is reached. In this way, the mixed-dimensional embeddings are automatically obtained. In the retraining stage, since feature interaction operations (e.g., the dot product) require embeddings to have the same dimension, we propose to utilize additional transform matrices to align dimensions for all fields, as shown in Figure 1(c). In this way, the obtained mixed-dimensional embeddings could be seamlessly integrated into architectures of traditional base models, which can be retrained in a standard way. The detailed procedures of SSEDS are summarized in Algorithm 1.

3.2.1 Pretraining. It is worth noting that SSEDS is model-agnostic, which can be employed to various recommendation models like FM [24], Wide&Deep [3] and DeepFM [9]. Therefore, we will not roll out the details of these uniform-dimensional recommendation methods. Instead, we will introduce the general training steps of these models. Specifically, we need to pretrain a complete recommendation model in a number of iterations before pruning, which aims at making the elements in the embedding table expressive. The forward pass procedures of the base recommendation model are abstracted as three layers including the embedding layer, the feature interaction layer, and the prediction layer.

For each training instance \((x, y)\), the embedding layer takes the raw features \(x = \{x_1, x_2, ..., x_n\}\) as inputs, and maps it into the embeddings \(e = \{e_1, e_2, ..., e_m\}\) in a field-wise manner via the Formula (2):

\[
e_i \in \mathbb{R}^{d_i}\]

where \(d_i\) is the embedding dimension for each field based on its influence on the loss function. Then the saliency scores are ranked in descending order.

3.2.2 Single-shot Pruning. Recall that the EDS problem could be transformed into the embedding pruning problem, i.e., identifying and removing those relatively unimportant dimensions of embeddings such that mixed-dimensional embeddings are automatically obtained. Hence, the critical problem is identifying the importance (a.k.a. saliency scores) for each dimension. Existing methods [20, 29] introduce the additional mask layer with learnable threshold parameters to learn the importance of embedding dimensions. However,
they need alternatively optimize threshold parameters and parameters of the model itself, resulting in expensive training processes. Inspired by SNIP [15], we introduce a saliency criterion to identify the importance of each embedding dimension of \( \hat{V}_i \) for each field \( i \in \{1, \ldots, m\} \) and each dimension \( j \in \{1, \ldots, d\} \) independently. In particular, we introduce an auxiliary indicator layer with binary parameters \( \alpha = \{\alpha_1, \alpha_2, \ldots, \alpha_m\} \), \( \alpha_i \in \{0,1\}^{d \times n_i} \). Then, for the desired parameter budget \( \kappa \), we can reformulate the objective function listed in Equation (4) as follows:

\[
\min_{\hat{V}, \hat{\alpha}} L(\hat{V} \odot \hat{\alpha}, \hat{\Theta}; D) \quad \text{s.t.} \quad \alpha \in \{0,1\}^{d \times \sum n_i}, \|\alpha\|_0 < \kappa \|\hat{V}\|_0
\]

where \( \odot \) represents the Hadamard product. Compared to Equation (4), we introduce additional indicator parameters \( \alpha \) which have the same size as \( \hat{V} \). However, we do not attempt to directly optimize Equation (8) but leverage \( \alpha \) to determine the importance of each embedding dimension. To be specific, we can measure the effect of the \( j \)-th dimension of the \( i \)-th field on the loss function independently by masking it while keeping embedding values of other dimensions unchanged, and measure the change of the loss value, which is formulated as follows:

\[
\Delta L_{i,j} = L(\hat{V} \odot \hat{\alpha}, \hat{\Theta}; D) - L(\hat{V} \odot (1 - \epsilon_{i,j}), \hat{\Theta}; D)
\]

where \( \epsilon \) is an all-1 matrix with dimension \( \sum n_i \times d \), and indicator matrix \( \epsilon_{i,j} \in \{0,1\}^{n_i \times d} \) is a binary matrix with value zero everywhere except for the position on the \( j \)-th dimension of the \( i \)-th field. However, computing all \( \Delta L_{i,j} \) is prohibitively expensive, which requires \( m \) forward passes over the dataset. On the other hand, \( L \) is not differentiable with respect to \( \alpha \). Inspired by the approximations in [14, 15], we relax the binary constraint of \( \alpha \) to continuous range \([0,1]\) such that \( \Delta L_{i,j} \) can be approximated by the gradients \( \partial L / \partial \alpha_{i,j} \) (denoted as \( g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b) \)) at the stationary point \( \alpha = 1 \):

\[
\Delta L_{i,j} \approx g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b) = \left. \frac{\partial L(\hat{V} \odot \alpha, \hat{\Theta}; \hat{D}_b)}{\partial \alpha_{i,j}} \right|_{\alpha=1} = \lim_{\delta \rightarrow 0} \frac{L(\hat{V} \odot (\alpha - \delta \epsilon_{i,j}), \hat{\Theta}; \hat{D}_b) - L(\hat{V} \odot \alpha, \hat{\Theta}; \hat{D}_b)}{\delta}_{\alpha=1}
\]

In this way, we can efficiently compute all \( g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b) \) via only one forward-backward pass using automatic differentiation on a mini-batch of dataset \( D \), denoted as \( \hat{D}_b \). Here, a larger magnitude of \( |g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b)| \) means that the corresponding dimension has a greater impact on the loss function (either positive or negative), and should therefore be retained. Based on this hypothesis, the saliency score \( s_{i,j} \) of the \( j \)-th dimension of the \( i \)-th field is defined as the normalized magnitude of \( |g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b)| \) as below:

\[
s_{i,j} = \frac{|g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b)|}{\sum_{i=1}^{m} \sum_{j=0}^{d} |g_{i,j}(\hat{V}, \hat{\Theta}; \hat{D}_b)|}
\]

After obtaining all saliency scores \( s_{i,j} \), we rank them in descending order, and then sequentially remove dimensions with low saliency scores until the parameter budget \( \kappa \) is reached. Precisely, the \( \alpha_{i,j} \) is computed as follows:

\[
\alpha_{i,j} = I(s_{i,j} - \hat{s} \geq 0), \forall i \in \{1, \ldots, m\}, j \in \{1, \ldots, d\}
\]  

\[
s.t. \|\alpha\|_0 < \kappa \|\hat{V}\|_0
\]

where \( I(\cdot) \) is the indicator function, and the quantile value \( \hat{s} \) is automatically determined based on the parameter budget.

It is worth noting that the above pruning method differs from the original network pruning method [15] in two ways. (1) We perform the single-shot pruning operation after pretraining, instead of prior to training as in the original one. The reason is that the embedding tables are independent of the model architecture, which prevents us from leveraging the architecture characteristics to perform pruning at the initialization stage. (2) Unlike the original one performing pruning at the weight level, which is analogous to pruning at the feature level in our context, we prune the embedding at the field level. The reason is that pruning at the feature level requires that the limited data in \( D_b \) must cover all unique features, which is hard to be satisfied due to sparsity and long-tail characteristics of features in recommender systems.

3.2.3 Retraining. After pruning, the mixed-dimensional embedding table \( \hat{V} = [\hat{V}_1, \ldots, \hat{V}_q]_{q \leq m}^{2} \), \( \hat{V}_i \in \mathbb{R}^{d_i \times n_i} \), are automatically obtained, where \( d_i \) is the searched dimension for the \( i \)-th field, and \( q \) is the number of fields after pruning. However, traditional recommendation models such as FM [24] and DeepFM [9] require the dimensional consistency among input embeddings due to feature interaction operations (e.g., the dot product). In order to make the pruned embeddings be seamlessly integrated into various model architectures. We need to align embedding dimensions among different fields, which has been studied in previous works. For example, FmFM [26] introduces additional \( \frac{d(d-1)}{2} \) matrices to align the dimensions for each pair of embeddings from different fields. Differently, inspired by the work in [11, 33], we utilize a simple yet effect method to align the dimension. Specifically, we only introduce \( q \) field-wise transform matrices \( M = \{M_1, \ldots, M_q\} \), \( M_i \in \mathbb{R}^{d_{max} \times d_i} \), where \( d_{max} = \max(d_1, \ldots, d_q) \) is the aligned embedding dimension equaling to the maximum dimension among all searched dimensions. Thus, we can get the aligned embedding \( \hat{e}_i \in \mathbb{R}^{d_{max}} \) for feature \( x_i \) as below:

\[
\hat{e}_i = M_i \hat{V} x_i
\]

Notice that we only introduce a tiny number of additional parameters, far less than those reduced embeddings. What’s more, \( M_i \) can boost the representation of the pruned embeddings \( \hat{V} \). 1) they are projected into a high-dimensional space with more perspectives for expression 2) \( M_i \) is shared for all feature instances in field \( i \), and thus their common attributes can be further modeled. After alignment, the dot product operation \( \langle \cdot, \cdot \rangle \) of traditional recommendation models between features in the \( i \)-th field and the \( j \)-th field can be performed as follows:

\[
\langle \hat{e}_i, \hat{e}_j \rangle
\]

Besides dot product operation, the pruned embeddings are also easily adaptable to other feature interaction operations. For example, the DNN layer [3, 9] only needs to adjust the dimension of the
input layer to match the dimension of the output of the embedding layer.

After aligning, we need to retrain the pruned embedding table \( \tilde{V} \), transform matrices \( M \), and other model parameters \( \tilde{\Theta} \) of the resulting slim model. According to the Lottery Ticket Hypothesis [7], there exists a sub-model whose accuracy can match the original model after training for the same number of steps from scratch, and such a sub-model is called the Winning Ticket. Moreover, compared to random initialization, restoring the parameters of the sub-model from the original well-trained model can further boost the performance. This theory inspires us to initialize the slim model using the pruned embedding table \( \tilde{V} \), and randomly initialize other model parameters, i.e., \( M \).

Algorithm 1 The proposed SSEDS algorithm

Require: Training dataset \( \mathcal{D} \), base model \( f(V, \Theta) \), parameter budget \( \kappa \), and loss function \( \mathcal{L} \).
Ensure: Mixed-dimensional embedding table \( V^* \) s.t. \( \|V^*\|_0 < \kappa \) \( \|V\|_0 \).

Pretraining:

Optimize \( V \) and \( \Theta; \tilde{V}, \tilde{\Theta} \leftarrow f \) \( V, \Theta \) by the base model \( f \).

Single-shot Pruning

Sample a mini-batch dataset \( \mathcal{D}_b \sim \mathcal{D} \)
Identify the saliency score \( s_{ij} \) for the \( j \)-th dimension of the \( i \)-th field \( \triangleright \) Equation (11)
Rank \( s_{ij} \) in descending order
Prune embedding table \( V \leftarrow \tilde{V} \) \( \triangleright \) Equation (12)

Retraining

Align the embedding dimension \( \triangleright \) Equation (13)
Retrain the slim model \( V^*, \tilde{\Theta} \leftarrow \tilde{V}, \tilde{\Theta} \).

4 EXPERIMENTS

In this section, we conduct extensive experiments aiming to answer the following research questions (RQs):

- **RQ1**: How does the proposed SSEDS perform under the different parameter budgets compared to other state-of-the-art methods?
- **RQ2**: Can the proposed SSEDS improve both the search efficiency of embedding dimensions and the inference efficiency of the model?
- **RQ3**: How does the proposed SSEDS perform on the practical recommender system in the industry?
- **RQ4**: How do the different components (e.g., retraining and Winning Ticket) affect the performance of the proposed SSEDS?
- **RQ5**: Is it necessary to prune most of the embeddings?

4.1 Experimental Setups

4.1.1 Datasets. The offline experiments are conducted on two widely used public datasets (i.e., Criteo and Avazu). Both of them are randomly split into training/validation/test sets as ratio 8:1:1, and the detailed information of datasets is summarized in Table 1.

| Dataset | #Instances | #Fields | #Features |
|---------|------------|---------|-----------|
| Criteo  | 46M        | 39      | 1M        |
| Avazu   | 40M        | 22      | 0.6M      |

- **Criteo**: It is a real-world industry dataset for CTR prediction, which consists of 45 million users’ click records on ads over one month. Each click record contains 13 numerical feature fields and 26 categorical feature fields. Following the winner of Criteo Competition\(^3\), we group those low-frequency (less than 10) features as a single feature ‘others’, and the numerical feature is transformed by \( \log(x) \), if \( x > 2 \).
- **Avazu**: It consists of 40 million users’ click records on ads over 11 days, and each record contains 22 categorical features. We use the pre-processing method as Criteo for the low-frequency features (less than 10) in Avazu.

4.1.2 Baselines. We compare the proposed SSEDS with the following state-of-the-art methods including uniform-dimensional methods such as FM [24], DeepFM [9] and Wide&deep [3], as well as different kinds of EDS methods including the heuristic based method (i.e., MDE [8]), the HPO based method (i.e., AutoDim), and embedding pruning based methods (i.e., PEP [20] and Deeplight).

- **Base methods**: We select representative CTR models including FM [24], DeepFM [9] and Wide&deep [3] as base models. These methods utilize uniform embedding dimension for all feature fields.
- **MDE [8]**: MDE (short for Mixed Dimension Embedding) is the method that heuristically sets embedding dimensions based on features’ popularity by human-designed rules.
- **AutoDim [33]** AutoDim utilizes a soft and continuous manner to calculate the weights over various dimensions for feature fields. Then the embedding architecture is derived from the maximum weight.
- **PEP [20]**: PEP is an embedding pruning based method for embedding dimensions search, which utilizes learnable thresholds to automatically prune redundant feature parameters so that sparse embeddings can be obtained adaptively.
- **Deeplight [5]** Deeplight proposes to prune both parameters in the embedding and DNN layers to solve the high-latency issues in CTR prediction.

4.1.3 Hyperparameters: The hyperparameters of the proposed SSEDS are set as follows. The initial embedding dimensions (i.e., in the pretraining stage) are 128 for all feature fields, and the parameter budget \( \kappa \) is 0.1 in the pruning stage. For deep layers, they contain 2 fully connected hidden layers with 1024 units in each layer, and the activation function for the layer’s outputs is \( \text{ReLU}(\cdot) \). We utilize Adam optimizer [13] with an initial learning rate 0.001 throughout the experiments, and the batch size is set to 2048 for all datasets. The baselines (i.e., MDE, PEP, and Deeplight) are implemented by

\(^3\)https://www.kaggle.com/c/criteo-display-ad-challenge
\(^4\)https://www.csie.ntu.edu.tw/20r01922136/kaggle-2014-criteo.pdf
\(^5\)https://www.kaggle.com/c/avazu-ctr-prediction
the codes provided by the authors. For a fair comparison, we set the initial (maximum) embedding dimension as 128 for all baseline models. All the offline experiments are run on a single machine with 2 Tesla P100 GPU with 32G memory.

4.1.4 Evaluation metrics: The CTR prediction task can be viewed as the binary classification (i.e., click and not click) task. Thus, we utilize the common metric [38], i.e., AUC (Area Under the ROC Curve) to evaluate the recommendation performance of all methods. On the other hand, we also count the number of model parameters, denoted as \( \#\text{Parameter} \), to measure model space complexities.

4.2 CTR Prediction (RQ1)

To validate the effectiveness of the proposed SSEDS, we compare it with other baselines on CTR prediction tasks. Specifically, the automated embedding dimension search methods (i.e., MDE, AutoDim, PEP, Deeplight, and proposed SSEDS) are regarded as plugins integrated into three base models (i.e., FM, DeepFM, and Wide & Deep) respectively. Furthermore, in order to validate the model performance under different parameter budgets \( \kappa \), we vary \( \kappa \) from 0.1 to 0.9 with step size 0.1 and 0.2 for the proposed SSEDS and the Deeplight respectively. For the PEP, we report its performance under three different sparsity levels. We only report the final optimized results for MDE and AutoDim due to their model characteristics. For base models, we set dimensions as \{32, 64, 128\}, and report their performance. The experimental results are shown in Figure 2 and Figure 3 for Criteo and Avazu, respectively, from which we can observe that:

- As the dimension increases, all base models can significantly achieve better performance on both datasets. It indicates that uniformly increasing dimensions for all feature fields could enhance the expression of the embeddings, resulting in better recommendation performance.
- The EDS based methods (i.e., MDE, AutoDim, PEP, Deeplight, and SSEDS) perform better than uniform embedding dimension based methods (i.e., FM, DeepFM, and Wide&Deep), which identifies that assigning the same embedding dimension for all feature fields is sub-optimal.
- The embedding pruning based EDS methods (i.e., PEP, Deeplight, and SSEDS) can achieve better performance than the heuristic based method (i.e., MDE) and the HPO based method (i.e., AutoDim) in most cases on both datasets. The possible reason is that embedding pruning based methods measure the importance of different dimensions at a finer-grained level (i.e., the embedding level), rather than at an upper level (i.e., the dimension level) as in heuristic and HPO methods.
- SSEDS is capable of significantly improving the performance of all base models by integrating searched mix-dimensional embeddings into them. For example, it improves the performance of DeepFM by 1.7% and 4.3% with respect to AUC scores, while reducing 90% embedding parameters on the Criteo and Avazu datasets, respectively. It is worth noting that merely 1% improvement is meaningful because of the large user base of businesses [3, 9].
- Under the various parameter budgets, the proposed SSEDS outperforms other EDS based methods on both datasets. We attribute such advances to the proposed saliency criterion that could explicitly identify the importance of each embedding dimension. Thus, the overall performance demonstrates the effectiveness and superiority of the proposed SSEDS.

4.3 Efficiency Analysis (RQ2)

It is inevitable to cost additional time to search for suitable embedding dimensions for different features. Thus, we study the time costs of the training stage (i.e., including pretraining, embedding dimension search, and retraining stages) on the training set, as well as the inference stage on the whole test set. Specifically, we set the training epochs as 3 for all methods for a fair comparison. Experimental results are shown in Figure 4 and Figure 5 respectively, and we can find out that:

- The proposed SSEDS spends the least additional time for the training stage, which is reasonable since SSEDS only need to prune the embeddings once after the pre-training, rather than requiring iterative optimization procedures in other EDS methods.
- The EDS based methods could significantly reduce the inference time compared to base models due to reducing a large number of redundant embeddings. Furthermore, the inference time of SSEDS is comparable with other EDS methods due to the similar number of parameters. Thus, the overall performance of SSEDS in terms of efficiency, especially the training efficiency, is superior to other methods.

4.4 Online A/B Test Experiment (RQ3)

To validate whether SSEDS could improve the performance while reducing the number of parameters on the practical recommender system in the industry, we deploy the SSEDS with a parameter budget 0.1 on the WeChat Subscription recommendation platform that covers hundreds of millions of users and generates hundreds of billions of click records every day. This online recommendation service aims to recommend a set of videos that users are most likely to click. We conduct a 7-day online A/B test experiment on this platform. Specifically, the base model is DeepFM [9] that has already been deployed on the WeChat Subscription platform, where about 3% of all users are set for the experimental group (SSEDS) and reference group (DeepFM), respectively. Both DeepFM and SSEDS are in an incrementally training manner every hour. We report the CTR (%) values and corresponding the number of parameters of the two models for each day in Figure 6. From the results, we can observe that:

- SSEDS could significantly improve about 4% of online CTR metric while reducing nearly 90% parameters, which confirms the practicality of SSEDS for the recommender system in the industry.
- With the continually incremental training, there is a growing trend of improvement, which demonstrates that the proposed method could well capture the dynamic changes of the data distribution. It is meaningful because the data distribution constantly changes in a real industrial scenario.

4.5 Ablation Study (RQ4)

This subsection aims to explore the effects of retraining and the Winning Ticket. The experiments are conducted on the Criteo and Avazu datasets for the CTR prediction task, and take DeepFM as the base model. In particular, we first explore the effect of retraining,
denoted as SSEDs w/o retraining, which implements the SSEDs without retraining. That is, we only use the embeddings from the pretrained model, and then prune the abundant dimensions via single-shot pruning. The randomly initialized transform matrices are utilized to align the dimension for different fields. We then explore the effect of the Winning Ticket. Recall that we use the pruned embeddings (i.e., the Winning Ticket) as the initial embeddings for the retraining stage. Thus, we explore its effect by random initialization in the retraining stage, denoted as SSEDs w/o ticket. Other settings are the same as the above experiments. The experimental results are shown in Table 2, we can observe that:

- SSEDs without retraining (i.e., SSEDs w/o retraining) degrades the model performance of SSEDs, but is still better than the base model on both two datasets. The possible reason is that over-parameterized embeddings might introduce noise or result in overfitting, which in turn demonstrates the necessity of embedding pruning.
- SSEDs retraining with random initialization (i.e., SSEDs w/o ticket) also degrades the model performance of SSEDs, but still achieves better performance than the base model and SSEDs w/o retraining. It implies that the Winning Ticket could improve the recommendation performance of the model.

### Table 2: The ablation study results with respect to the retraining and the Winning Ticket.

| Methods         | Criteo  | Avazu  |
|-----------------|---------|--------|
| Base (DeepFM)   | 0.8017  | 0.78   |
| SSEDs w/o retraining | 0.8020  | 0.7812 |
| SSEDs w/o ticket | 0.8027  | 0.7826 |
| **SSEDs**       | **0.8031** | **0.7834** |

### 4.6 Pruning Results Analysis (RQ5)

To further demonstrate the necessity of embedding pruning, we present the distribution of saliency scores as well as the searched dimensions under the parameter budget $k = 0.1$. The experimental results are shown in Figure 7 and Figure 8 for Criteo and Avazu datasets, respectively. We can observe that:

- For both datasets, the saliency scores obey the power-law distribution, i.e., only a tiny proportion of dimensions have a large effect on the loss function. Such results are consistent with the characteristic of features in the recommender system, i.e., features following the long-tail distribution [12, 23]. Thus, it is reasonable and necessary to prune most of the embedding parameters.
- Only a small portion of feature fields are assigned with relatively large dimensions, while most of the fields are assigned small dimensions, or even 0 dimensions (meaning that the corresponding field is removed). It demonstrates that our method could also be utilized as an effective technique for automatic feature selection.

### 5 CONCLUSION

In this paper, we have modeled the EDS problem in the recommender system as the embedding pruning problem, where the suitable embedding dimensions for different feature fields could be automatically obtained by removing those relatively unimportant dimensions under the desired parameter budget. To achieve this goal, we proposed a single-shot embedding dimension search method, termed SSEDs, which introduces a saliency criterion for identifying the importance of embedding dimensions in an efficient way. Extensive offline experiments have been conducted to validate the effectiveness and efficiency of the proposed SSEDs on two widely used datasets. The experimental results have shown that the proposed SSEDs can achieve better recommendation performance than both the traditional uniform dimension based methods and recent EDS based methods while reducing a large number of embedding parameters (about 90%). On the other hand, the efficiency of embedding dimensions search for SSEDs is superior to other methods. Furthermore, the proposed SSEDs has also been deployed on the WeChat Subscription platform for online recommendation services. The 7-day A/B test results have demonstrated that SSEDs could significantly improve the performance of the online recommendation model while reducing resource consumption.

In the future, we plan to employ the proposed SSEDs to different recommendation tasks and explore how to leverage the prior knowledge of features to improve the model performance further. Furthermore, we will also explore to search embedding dimensions in a dynamic situation [22].
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