[C II] 158 µm line emission from Orion A.
I. A template for extragalactic studies?

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ABSTRACT

Context. The [C II] 158 µm fine-structure line emission is one of the dominant coolants of the neutral interstellar medium. It is hence one of the brightest far-infrared emission lines and can be observed not only in star-forming regions throughout the Galaxy, but also in the diffuse interstellar medium and in distant galaxies. [C II] line emission has been suggested to be a powerful tracer of star-formation.

Aims. We aim to understand the origin of [C II] emission and its relation to other tracers of interstellar gas and dust. This includes a study of the heating efficiency of interstellar gas as traced by the [C II] line to test models of gas heating.

Methods. We make use of a one-square-degree map of velocity-resolved [C II] line emission towards the Orion Nebula complex, including M43 and NGC 1977. We employ Herschel far-infrared photometric images to determine dust properties. Moreover, we compare with Hα emission from the ionized gas, Spitzer mid-infrared photometry to trace hot dust and large polycyclic aromatic hydrocarbons (PAHs), and velocity-resolved IRAM 30m CO(2-1) observations of the molecular gas.

Results. The [C II] intensity is tightly correlated with PAH emission in the IRAC 8 µm band and far-infrared emission from warm dust. However, the [C II] intensity depends less than linear on the 8 µm and far-infrared intensity, while 8 µm- and far-infrared intensities are approximately linearly correlated. The correlation between [C II] and CO(2-1) does not show a clear trend and is affected by the detailed geometry of the region. We find particularly low [C II]-over-FIR intensity ratios towards large columns of (warm and cold) dust, which suggest the interpretation of the “[C II] deficit” in terms of a “FIR excess”. A slight decrease in the FIR line-over-continuum intensity ratio can be attributed to a decreased heating efficiency of the gas. Furthermore, we find that, at the mapped spatial scales, predictions of the star-formation rate from [C II] emission, like most other tracers, underestimate the star-formation rate calculated from YSO counts in the Orion Nebula complex by an order of magnitude.

Conclusions. [C II] emission from the Orion Nebula complex arises dominantly in the cloud surfaces, many viewed in edge-on geometry. Most of the [C II] emission stems from the extended fainter outskirts of the irradiated regions, while the [C II] intensity is deficient with respect to the total far-infrared intensity in the brightest regions. [C II] emission from extended faint cloud surfaces may contribute significantly to the total [C II] emission on galactic scales.

Key words. Infrared: ISM – ISM: structure – ISM: individual objects: M42, M43, NGC 1977

1. Introduction

The [C II] 158 µm fine-structure line dominates the far-infrared (FIR) spectrum of the Milky Way, carrying up to 1% of the total luminosity (Bennett et al. 1994). Given the small energy separation of the two line structure-levels (∆E = 91.2 K), low critical density (several 10^3 cm^{-3} for collisions with hydrogen atoms; e.g., Goldsmith et al. 2012), and the high abundance of carbon, this transition is the dominant cooling line of diffuse atomic gas (Dalgarno & McCray 1972), the so-called cold neutral medium phase of the interstellar medium (ISM). In the surfaces of molecular clouds, the CO molecule is photodissociated and carbon is singly ionized (ionization potential of 11.3 eV) by the interstellar radiation field. This so-called CO-dark (atomic and) molecular gas (Grenier et al. 2005; Wolfire et al. 2010) also radiates substantially in the [C II] line (e.g., Langer et al. 2010). Also in regions of massive star formation, the strong UV field photod dissociates molecules, ionizes atoms, and heats the gas. These dense photodissociation regions (PDRs) emit bright atomic fine-structure lines. In particu-
lar, the [C\textsc{ii}] 158\,\mu m line and the [O\textsc{i}] 63\,\mu m and 145\,\mu m lines (at high gas densities) are the main gas coolants (Hol- lenbach & Tielens 1999). Finally, the [C\textsc{ii}] line can also arise from low-density regions of ionized gas, such as the warm ionized medium (Heiles 1994). Observational studies have demonstrated that each of these ISM components contributes to the [C\textsc{ii}] emission of the Milky Way (e.g., Stacey et al. 1991; Shibai et al. 1991; Bennett et al. 1994; Bock et al. 1993; Abdullah & Tielens 2020). In particular, the pencil-beam Herschel/HIFI GOTC+ [C\textsc{ii}] survey suggests that much of the observed [C\textsc{ii}] emission in our Galaxy emerges from dense PDRs (~47\%), with smaller contributions from CO-dark molecular gas (~28\%), cold atomic gas (~21\%), and ionized gas (~4\%; Pineda et al. 2013).

Irrespective of its origin, the [C\textsc{ii}] emission is linked to the presence of stellar far-ultraviolet photons (FUV; \(E < 13.6\text{eV}\)). As FUV photons are tied to the presence of massive O and B stars that have short lifetimes, the [C\textsc{ii}] 158\,\mu m line is also a star formation rate indicator. Indeed, ISO, Herschel and SOFIA observations have demonstrated the good correlation between the [C\textsc{ii}] luminosity and the star-formation rate (SFR) in the Milky Way and in regions of massive star formation in other galaxies (e.g., Kramer et al. 2013, 2020; Pineda et al. 2014, 2018; Herrera-Camus et al. 2015, 2018; De Looze et al. 2011).

With ALMA and NOEMA, ground-based observations of the [C\textsc{ii}] 158\,\mu m line in high redshift galaxies has come into reach and such data is routinely used to infer star formation rates (e.g., Walter et al. 2012; Venemans et al. 2012; Knudsen et al. 2016; Bischoff et al. 2018; Khulanova et al. 2020) based upon validations of this relationship in the nearby Universe (Herrera-Camus et al. 2018; De Looze et al. 2011). However, it is well-understood that the intensity of the [C\textsc{ii}] line depends on the local physical conditions (Hollenbach & Tielens 1999). Observationally, the presence of the so-called “[C\textsc{ii}]-deficit” – a decreased ratio of [C\textsc{ii}] 158\,\mu m luminosity to FIR dust continuum with increasing dust color temperature and also with FIR luminosity – is well established (Malhotra et al. 2001; Díaz-Santos et al. 2013; Magdis et al. 2014; Smith et al. 2017). This deficit is particularly pronounced in (local) ultraluminous infrared galaxies (ULIRGs), very dusty galaxies characterized by vigorous embedded star formation (e.g., Luhman et al. 2003; Abel et al. 2009; Graciá-Carpio et al. 2011). This deficit, however, does not necessarily hold in the early Universe at high redshift (e.g., Goicoechea et al. 2015; Pabst et al. 2019). For example, [C\textsc{ii}] emission seen around the Horsehead Nebula (in Orion B, about 3° north of Orion A; Pabst et al. 2017; Bally et al. 2018) and with the [C\textsc{ii}] emission imaged over the entire nearby spiral galaxy M51 (Pineda et al. 2018), both mapped by SOFIA.

This study is organized into a series of two papers. In this paper (Paper I), we examine the relationship between the [C\textsc{ii}] emission and other observational tracers of star formation, as well as the implications for the [C\textsc{ii}] deficit, using the square-degree observations of Orion carried out with SOFIA/upGREAT (for details see Pabst et al. 2019, 2020). In a second paper (Paper II), we investigate the correlations in more detail, relate them to small-scale emission features and PDR physics, and compare with detailed PDR models. This paper is organized as follows: In Section 2, we will briefly describe the observations used in this study. Section 3 discusses the global morphology of the [C\textsc{ii}] line emission and presents the correlations we find of the [C\textsc{ii}] emission with other tracers of gas and dust in the Orion Nebula complex. In Section 4, we discuss the implications of the results of Section 3 and the relation between [C\textsc{ii}] emission and the star-formation rate. We summarize our results in Section 5.

2. Observations

2.1. [C\textsc{ii}] observations

We use the same velocity-resolved [C\textsc{ii}] line observations as Pabst et al. (2019, 2020). Details of the observing strategy and data reduction are provided by Higgins et al. (2021). The [C\textsc{ii}] 158\,\mu m line observations towards the Orion Nebula complex, covering M42, M43 and NGC 1973, 1975, and 1977, were obtained during 13 flights in November 2016 and February 2017 using the 14-pixel high-spectral-
resolution heterodyne array of the German Receiver for Astronomy at Terahertz Frequencies (upGREAT) onboard the Stratospheric Observatory for Infrared Astronomy (SOFIA). We obtained a fully-sampled map of a 1.2 square-degree-sized area at an angular resolution of 16″ using the array on-the-fly (OTF) mode. The resulting root-mean-square noise per pixel at a spectral resolution of 0.3 km s$^{-1}$ resulted in $T_{\text{mb}} \approx 1.14$ K after re-binning the original data with a natural spectral resolution of 0.04 km s$^{-1}$. For the baseline removal, a catalogue of splines was produced from spectra not containing an astronomical signal, and those were scaled to the astronomical data. The repeatability between flights is 7% (Higgins et al. 2021), and we take this as an estimate of the intensity uncertainty.

2.2. CO(2-1) observations

We also make use of $^{12}$CO $J = 2-1$ (230.5 GHz) and $^{13}$CO $J = 2-1$ (220.4 GHz) line maps taken with the IRAM 30 m radiotelescope (Pico Veleta, Spain). The central region (1′ × 0.8″) around OMC1 was originally mapped in 2008 with the HERA receiver array, and the mapping and data reduction strategies were presented by Berné et al. (2014). These CO maps with a native angular resolution of 0.7′′ were enlarged using the new EMIR receiver and FFTS backends. The fully-sampled maps are part of the Large Program “Dynamic and Radiative Feedback of Massive Stars” (Goicoechea et al. 2020) give details on how the old HERA and new EMIR CO maps were merged and on the conversion from antenna temperature to main-beam temperature. The typical root-mean-square noise in the CO(2-1) map is $T_{\text{mb}} \approx 0.16$ K at a spectral resolution of 0.4 km s$^{-1}$. The IRAM Large Program is an ongoing survey and we use the data as available in March 2020. Specifically, coverage in NGC 1977 is not complete and the newly observed data will be the subject of a future paper.

2.3. Dust SEDs

We use the dust SEDs in the Orion Nebula complex described in Pabst et al. (2020). They use the Herschel/PACS and SPIRE photometric images of the dust FIR continuum to determine the effective dust temperature and the dust optical depth, and fit a modified blackbody,

$$I_\lambda = B(\lambda, T_d) \left[ 1 - \exp \left( -\tau_{160} \left( \frac{160 \mu m}{\lambda} \right)^{\beta} \right) \right],$$

with dust emissivity index $\beta = 2$ to the three PACS 70 μm, 100 μm, and 160 μm bands, and three SPIRE 250 μm, 350 μm, and 500 μm bands, convolved and re-gridded to the resolution of the SPIRE 500 μm band with 36″ angular resolution and a pixel size of 14″. The brightest regions around the star-forming cores are saturated in the Herschel bands and hence excluded from our analysis.

The SED fits are biased towards the warm dust emission, and thus tend to underestimate the dust optical depth where colder dust is mixed in the line of sight. Moreover,

1. upGREAT is a development by the MPI für Radioastronomie and KOSMA/Universität zu Köln, in cooperation with the DLR Institut für Optische Sensorsysteme.

2. The native resolution, before gridding, is 14.1″.
The distribution of various gas and dust tracers (FIR, CO(2-1), \(\text{H}^\alpha\)) delineate the three distinct shells of M42, M43, and NGC 1977. The stars indicate the most massive stars within each region: \(\theta^\prime\) Ori C (yellow) in M42, NU Ori (pink) in M43, and 42 Orionis (purple) in NGC 1977. Arrows indicate the positions of the four molecular cores OMC1-4 along the Integral-Shaped Filament.

### 3.1. Global morphology of the emission

Figure 1 shows the [C\textsc{ii}] line-integrated intensity from Orion A at its original resolution (16'). The red circles delineate the three distinct shells of M42, M43, and NGC 1977. The stars indicate the most massive stars within each region: \(\theta^\prime\) Ori C (yellow) in M42, NU Ori (pink) in M43, and 42 Orionis (purple) in NGC 1977. Arrows indicate the positions of the four molecular cores OMC1-4 along the Integral-Shaped Filament.

#### 3.2. Correlation plots of gas and dust tracers

| x     | y     | a     | b     | p      | \(\operatorname{rms}\) [dex] |
|-------|-------|-------|-------|--------|-----------------------------|
| 70 \(\mu\)m | [C\textsc{ii}] | 0.57 ± 0.31\(^a\) & -5.10 ± 1.02 & 0.90 & 0.13 |
| FIR   | [C\textsc{ii}] | 0.60 ± 0.28\(^b\) & -2.61 ± 0.29 & 0.90 & 0.12 |
| 8 \(\mu\)m | [C\textsc{ii}] | 0.65 ± 0.30 & -1.83 ± 0.64 & 0.93 & 0.10 |
| 8 \(\mu\)m | FIR | 1.16 ± 0.37 & 1.43 ± 0.77 & 0.94 & 0.16 |
| CO(2-1) | [C\textsc{ii}] | 0.96 ± 0.63 & 2.39 ± 3.89 & 0.53 & 0.37 |
| CO(2-1) | FIR | 0.71 ± 0.60 & 1.24 ± 2.85 & 0.34 & 0.29 |

#### Notes.

The regression fitted to the data in a weighted least-square fit is \(\log_{10} y = a \log_{10} x + b\). Fit in [C\textsc{ii}] > \(3\sigma\) \(\simeq 5 \times 10^{-5} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\), \(I_{70\mu m} > 5 \times 10^{4} \text{ MJy} \text{sr}^{-1}\), \(I_{\text{FIR}} > 3 \times 10^{-3} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\), and/or \(I_{\text{FIR}} > 3 \times 10^{-2} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\), \(\rho\) is the Pearson correlation coefficient, \(\operatorname{rms}\) is the root-mean-square of the residual of the fit. \(^a\) For \(I_{70\mu m} < 5 \times 10^{4} \text{ MJy} \text{sr}^{-1}\) we obtain \(a \simeq 1.10 \pm 0.68\) and \(b \simeq -6.45 \pm 1.61\) with \(\rho \simeq 0.67\) and \(\operatorname{rms} \simeq 0.18\). \(^b\) For \(I_{\text{FIR}} < 3 \times 10^{-2} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\) we obtain \(a \simeq 1.15 \pm 0.76\) and \(b \simeq -1.72 \pm 1.37\) with \(\rho \simeq 0.71\) and \(\operatorname{rms} \simeq 0.17\).

Figure 3 shows the point-by-point correlation between the different gas and dust tracers as density plots. Table I summarizes the power-law fits we find for each correlation, using the ordinary least-squares (OLS) bisector method (Isobe et al. 1990) on the logarithmic scale. We have included all points that lie above the \(3\sigma\) \(\simeq 8\text{ K km s}^{-1} \simeq 5 \times 10^{-5} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\) threshold of the [C\textsc{ii}] line-integrated intensity (after convolution). We do not apply this threshold to the FIR-8\(\mu\)m correlation, but we restrict both maps to the coverage of the [C\textsc{ii}] map. We subtract an offset of \(2 \times 10^{-3} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\) from the IRAC 8\(\mu\)m data. However, at low intensities we find 70\(\mu\)m and FIR emission that does not correspond to [C\textsc{ii}] emission. We fit this regime (\(I_{70\mu m} < 5 \times 10^{4} \text{ MJy} \text{sr}^{-1}\)) and/or \(I_{\text{FIR}} < 3 \times 10^{-2} \text{ erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}\) (respectively) separately. We point out that this low-intensity regime is problematic because of calibration uncertainties in the PACS bands, hence we will refrain from a detailed analysis thereof. The same holds for the IRAC 8\(\mu\)m map, where we cannot exclude that the offset we subtract has a physical reason. We caution that this has to be taken into account when estimating the [C\textsc{ii}] intensity from the IRAC 8\(\mu\)m intensity at low surface brightness.

The [C\textsc{ii}] intensity is tightly correlated with the intensity in the PACS 70\(\mu\)m band (Fig. 3a), the FIR intensity (Fig. 3b), and with the intensity in the IRAC 8\(\mu\)m band (Fig. 3c). The FIR intensity is also tightly correlated with the intensity in the IRAC 8\(\mu\)m band (Fig. 3d). The Pearson correlation coefficients (\(\rho\)) in panels a to d are about 0.9, while the scatter around the correlations is of the order 0.1-0.2 dex. Most important to note is that the correlation of the [C\textsc{ii}] intensity with each of the 70\(\mu\)m, FIR (in the...
high-intensity regime), and 8 µm intensity is not linear, but scales with those intensities to a power of less than unity. At low FIR intensity, the [C\textsc{ii}] intensity and the 8 µm intensity are largely independent of the FIR intensity.

The [C\textsc{ii}] and CO(2-1) correlations are more complex and require a more thorough analysis, which we will return to and follow up in Paper II. The [C\textsc{ii}]-low-J CO relationship, either as absolute intensities or normalized to the FIR intensity, is frequently used to infer physical conditions in Galactic and extragalactic star-forming regions (Wolff et al. 1989; Stacey et al. 1991; Herrmann et al. 1997), which is why we include it here. Collectively, the [C\textsc{ii}]-CO(2-1) correlations in Orion A (Figs. 3e and f) do not follow a simple power-law trend.

To estimate the FUV radiation field, we discuss briefly the FIR intensity as function of the distance from the massive star\textsuperscript{3} Figure 4 shows the dependence of the FIR intensity on distance from the central star\textsuperscript{4} Ori C in M42. We find a decline of the FIR intensity in accordance with geometric dilution, that is decreasing with the distance squared. The FIR intensity scales directly with the incident FUV radiation field, given as \( G_0 \) in units of the Habing field, typically \( G_0 \approx \frac{I_{\text{FIR}}}{2/1.3 \times 10^{-4} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1}} \), where the factor 1/2 accounts for the absorption of visible photons by dust (Hollenbach & Tielens 1999). However, geometry and line-of-sight effects are important, most of the sight lines being towards limb-brightened cloud edges. The true FUV field may be found by the lower intensities in the correlation of Fig. 3 as those correspond to the face-on background cloud and are not affected by limb brightening. This yields \( G_0 \approx 500 \) at a distance of 1 pc. Also following the prescription of Meixner et al. (1992), \( G_0 \approx L_{\text{FIR}}/(4\pi S) /2/1.3 \times 10^{-4} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \), where \( S \) is the surface that is exposed to the FUV radiation field, we obtain \( G_0 \approx 500 \) at a distance of 1 pc from the FIR luminosity of the edge-on eastern shell\textsuperscript{4}. From the total FIR luminosity of M42, \( 1.5 \times 10^3 L_\odot \) excluding the BN/KL and Orion S region, we estimate \( G_0 \approx 1500 \) at a distance of 1 pc. While, in principle, the incident radiation field can be estimated from the stellar luminosity and the (true) distance from the illuminating source, oftentimes only the projected distance is known. In the case of the Orion Nebula, the de-

\textsuperscript{3} We assume a distance of 414 pc to the Orion Nebula (Menten et al. 2007) to be consistent with Pabst et al. (2019, 2020). More recent observations suggest a slightly lower value (Kounkel et al. 2017, Grohschell et al. 2018).

\textsuperscript{4} We sum over an area of 3′ × 3′ in the limb-brightened eastern edge, obtaining \( L_{\text{FIR}} \approx 1.8 \times 10^3 L_\odot \). At a distance of 414 pc, 3′ ≈ 0.36 pc. The column exposed to the FUV radiation field has an approximate length of \( r/2 \approx 1.3 \text{ pc} \), where \( r \approx 2.5 \text{ pc} \) is the radius of the shell structure. Hence, \( S \approx 0.36 \text{ pc} \times 1.3 \text{ pc} \).
Fig. 3. Correlations of all map points as point-density plots: a) [C\textsc{ii}]-70\,\mu m, b) [C\textsc{ii}]-FIR, c) [C\textsc{ii}]-8\,\mu m, d) FIR-8\,\mu m, e) [C\textsc{ii}]-CO(2-1), f) [C\textsc{ii}]/FIR-CO(2-1)/FIR. The regression curve with parameters of Table 1 is drawn in the respective panels (solid lines; dashed lines in panels a and b are the regression curves in the low-intensity regime).

4. Discussion

The Orion A molecular cloud towards the Orion Nebula (NGC 1976 or M42) is the closest site of ongoing massive-star formation, and thus a perfect template to resolve the spatial distribution of the [C\textsc{ii}] emission. At a distance of 414 ± 7pc from the earth (Menten et al. 2007), it covers about one square degree on the sky. To the north of the Orion Nebula lies De Mairan’s Nebula (NGC 1982 or M43) and the Running-Man Nebula with NGC 1973, 1975, and 1977. The Orion Nebula itself is illuminated by the massive stars in the Trapezium cluster, the dominant star being...
the O7V star \( \bar{\theta} \) Ori C at only \( \sim 0.3 \) pc from the molecular cloud. According to the blister model (Zuckerman 1973 Balick et al. 1974), the environsing H\( \text{II} \) region, the so-called Huygens Region, is located in front of the background Orion A molecular cloud. This very central part of the cloud includes the Orion Molecular Core 1 (OMC1) that hosts the embedded massive-star forming clumps Orion BN/KL and Orion S (e.g., Grenz \& Stutzki 1989). OMC1 also hosts the famous Orion Bar, a FUV-illuminated edge of the molecular cloud, and an archetypical example of a strongly irradiated PDR (\( G_0 \approx 10^5 \)) that has been subject of many detailed studies (e.g., Tielens et al. 1993; Goicoechea et al. 2016). The H\( \text{II} \) regions of M43 and NGC 1977 are ionized by the B0.5V star NU Ori and the B1V star 42 Ori, respectively. All these regions are subject to ongoing dynamical evolution. M42 is surrounded by a stellar-wind driven shell expanding at 13 km s\(^{-1}\) (Pabst et al. 2019), filled with a photo-ionized medium (O’Dell \& Harris 2010) and an X-ray emitting hot plasma (Güdel et al. 2008). Both M43 and NGC 1973, 1975, and 1977 are surrounded by shells that expand under the influence of the contained over-pressurized ionized gas (Pabst et al. 2020).

### 4.1. Comparison with Orion B

An early spatial correlation study of the central OMC1/Huygens region (\( \sim 85 \) arcmin\(^{-2}\)) was carried out by Goicoechea et al. (2015b) using Herschel/HIFI. This region is very bright in the FIR and shows very low \([\text{C} \text{ii}]/\text{FIR}\) intensity ratios (approaching \( 10^{-4} \)) reminiscent of the “\([\text{C} \text{ii}]\) deficit” seen in local ULIRGs. These authors concluded that the low luminosity ratios in this particular region are produced by the very large column density of warm dust throughout the star-forming core. Here, we expand this correlation study to much larger spatial scales, encompassing a much wider range of physical conditions, dust column densities, and FUV radiation illumination. In order to include regions of very low \([\text{C} \text{ii}]\) surface brightness into the analysis, and to study the role of different environment/stellar-illumination conditions, we also incorporate the \([\text{C} \text{ii}]\) emission mapped by SOFIA around the Horsehead Nebula and adjacent IC 434 H\( \text{II} \) region (located in Orion B, about 3° north of Orion A; Pabst et al. 2017). This region in Orion B is illuminated by the multiple star system \( \sigma \) Ori, dominated by a massive star of spectral type O9.5V and located \( \sim 3 \) pc (in projection) from the Horsehead, producing \( G_0 \approx 100 \) at the surface of the molecular cloud (e.g., Abergel et al. 2003).

#### Table 2. Summary of the density correlation plots in Fig. 5

| \( x \) \( y \) \( a \) \( b \) \( \rho \) \( \text{rms} \) \( \text{dex} \) |
|---|---|---|---|---|---|---|
| \( 70 \) \( \mu \text{m} \) \([\text{C} \text{ii}]\) | \( 0.50 \pm 0.13 \) | \( -4.85 \pm 0.39 \) | 0.93 | 0.11 | |
| FIR \([\text{C} \text{ii}]\) | \( 0.56 \pm 0.15 \) | \( -2.65 \pm 0.20 \) | 0.94 | 0.11 | |
| 8 \( \mu \text{m} \) \([\text{C} \text{ii}]\) | \( 0.70 \pm 0.18 \) | \( -1.79 \pm 0.40 \) | 0.95 | 0.10 | |
| 8 \( \mu \text{m} \) FIR | \( 1.19 \pm 0.17 \) | \( 1.39 \pm 0.43 \) | 0.93 | 0.20 | |

**Notes.** The regression fitted to the data is \( \log_{10} y = a \log_{10} x + b \). Fit in \([\text{C} \text{ii}]\) only \( > 3 \sigma \) of the Orion B data, \( \rho \) is the Pearson correlation coefficient, \( \text{rms} \) is the root-mean-square of the residual of the fit.

Figure 5 compares the correlations of the \([\text{C} \text{ii}]\) intensity with the \( 70 \mu \text{m}, \) FIR, and 8 \( \mu \text{m} \) intensity, and the FIR-\( \mu \text{m} \) correlation in Orion A and B. For Orion A, we plot the data in M42 only (with \( I_{\text{[C} \text{ii}] < 2 \times 10^{-2} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \)). Data of Orion B are taken from Pabst et al. (2017) and plotted for \( I_{\text{[C} \text{ii}] > 3 \sigma \times 6 \times 10^{-5} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \). The correlations we find from the combined data sets, summarized in Table 2, are very similar to those found from the Orion A data only (cf. Table 1). The Orion A data form a perfect continuation of the earlier study of \([\text{C} \text{ii}]\) emission in Orion B, allowing us to extend the correlations over more than two orders of magnitude in \([\text{C} \text{ii}]\) intensity.

While Orion A is a region shaped by the stellar feedback from the locally formed massive stars, L1630 in Orion B is shaped by a chance encounter of a massive star with a molecular cloud. The O9.5V star \( \sigma \) Ori in Orion B is approaching the cloud and photovapourizing the gas from its surface (Ochsendorf et al. 2014). On the other hand, the shell structures that emit most of the \([\text{C} \text{ii}]\) luminosities in Orion A are created by the stars in their respective centers. Regardless of the formation history of the emitting gas structures, the \([\text{C} \text{ii}]\) intensity is determined by PDR physics, as the tight correlations with the FIR and 8 \( \mu \text{m} \) intensity, respectively, reveal.

#### 4.2. The \([\text{C} \text{ii}]\) deficit

Multiple studies of galaxies report that the \([\text{C} \text{ii}]\)/FIR ratio drops with increasing FIR luminosity and increasing FIR color temperature (e.g., Malhotra et al. 2001; Luhman et al. 2003). This is referred to as “\([\text{C} \text{ii}]\) deficit”. Usually, other FIR lines are affected, as well (e.g., Herrera-Camus et al. 2018). For the \([\text{C} \text{ii}]\) 158 \( \mu \text{m} \) line, in particular, emission may be suppressed and cooling could come out in, for example, the \([\text{O} \text{i}]\) 63 \( \mu \text{m} \) line (critical density of several \( 10^5 \) cm\(^{-3}\)) in dense PDRs. The photoelectric heating rate depends nonlinearly on the incident FUV radiation field at small dust grains and PAHs get charged at high radiation field, the relative contribution from different components of the ISM to the \([\text{C} \text{ii}]\) emission varies, and/or the FIR continuum emission has a large contribution from non-PDR dust. In (UL)IRGs, the \([\text{C} \text{ii}]\) deficit has been attributed to the importance of \([\text{O} \text{i}]\) cooling at high UV fields and densities as well as the importance of heating sources of dust other than stellar radiation (e.g., AGN activity Malhotra et al. 2001).
Fig. 5. Comparison of the correlations in Orion A and B: a) [C ii]-70 µm, b) [C ii]-FIR, c) [C ii]-8 µm, d) FIR-8 µm. The color scale in Orion A indicates the distance from θ^1 Ori C.

Luhman et al. 2003; Croxall et al. 2012; Pineda et al. 2018; Rybak et al. 2020b). In more distant high-mass star-forming regions and in distant galaxies, some of the low [C ii]/FIR ratios may be explained by [C ii] absorption by foreground diffuse gas, for example diffuse clouds in the spiral arms (Gerin et al. 2015). Nearby, well-resolved regions of massive star formation provide an ideal opportunity to study some of these effects in detail as any “deficit” can be linked to the characteristics of the source and the local physical conditions. The large-scale [C ii] map of the Orion Nebula complex allows us to address some of the issues that may influence the [C ii]/FIR ratio.

Figure 1 in Herrera-Camus et al. (2018) illustrates the [C ii] deficit in a local sample of archetypical galaxies. The authors note that the threshold value in FIR surface luminosity, above which the [C ii]/FIR ratio decreases, marks galaxies with $L_{\text{FIR}}/M_{\text{gas}} \gtrsim 50 L_\odot/M_\odot$. Values of $L_{\text{FIR}}/M_{\text{gas}} \approx 50$-80 $L_\odot/M_\odot$ have been suggested to characterize galaxies with enhanced star formation (e.g., Genzel et al. 2010). In the Orion Nebula complex, high values of $L_{\text{FIR}}/M_{\text{gas}}$ (computed from the dust SEDs and using standard dust properties of Weingartner & Draine 2001) are found towards OMC1 and close to the central stars of M43 and NGC 1977 (see Fig. 6). In fact, we can express the ratio as

$$L_{\text{FIR}}/M_{\text{gas}} \approx 4\pi \times 4 \times 10^{-2} \int_{40 \mu m}^{500 \mu m} B(\lambda, T_d) \left(\frac{160 \mu m}{\lambda}\right)^{\beta} d\lambda \frac{L_\odot}{M_\odot},$$

with $L_{\text{FIR}} = 4\pi A\tau_{160} \int_{40 \mu m}^{508 \mu m} B(\lambda, T_d)(160 \mu m/\lambda)^{\beta} d\lambda$ (in the optically thin limit) and $M_{\text{gas}} = 6 \times 10^{24} \text{cm}^{-2} \mu \text{m}_{\text{A}} A\tau_{160}$, where $A$ is the surface area, $\mu = 1.4$ the mean atomic weight, and $B(\lambda, T_d)(160 \mu m/\lambda)^{\beta}$ is the modified black-body function (cf. Eq. 1). In a second step, we approximate the integral over FIR wavelengths by the infinite integral $\int_{0}^{\infty} B(\lambda, T_d)(160 \mu m/\lambda)^{\beta} d\lambda \approx 4.17 \times 10^{-8} \text{erg s}^{-1} \text{cm}^{-2} \text{sr}^{-1} \text{K}^{-6} T_d^6$ for $\beta = 2$, and obtain

$$L_{\text{FIR}}/M_{\text{gas}} \approx 2 \times 10^{-2} \left(\frac{T_d}{10 K}\right)^6 \frac{L_\odot}{M_\odot}. \quad (3)$$

This is accurate for optically thin dust FIR emission and 10 K $\lesssim T_d \lesssim 35$ K. For $T_d = 40$ K, the finite integral is overestimated by 10%, and by 25% for $T_d = 50$ K. Below $T_d = 10$ K, the dust blackbody emission rapidly shifts towards millimeter wavelengths and the infinite integral is not a good approximation for the FIR emission either.5

5 If the FIR intensity includes the wavelength range 500-1000 µm, the infinite integral is accurate down to $T_d \sim 5$ K.
Expressed in this way, the ratio $L_{\text{FIR}}/M_{\text{gas}}$ is independent of the gas column and depends solely on the effective dust temperature. Naturally, the effective dust temperature in Orion A is highest towards the ionized gas, that is close to the central heating source. We show a map of the dust temperature in Paper II. In our SED fits, the molecular ridge with the BN/KL region and Orion S is excluded (for detailed SED fitting of this region, see Chuss et al. (2019)). $L_{\text{FIR}}/M_{\text{gas}}$ assumes peak values of $80 L_{\odot} M_{\odot}^{-1}$ in M42, $60 L_{\odot} M_{\odot}^{-1}$ in M43, and $20 L_{\odot} M_{\odot}^{-1}$ in NGC 1977 (with the exception of $40 L_{\odot} M_{\odot}^{-1}$ towards NGC 1973). These highest values are concentrated in the H II regions of M43 and NGC 1977, like in OMC1. From SED fits of Chuss et al. (2019), we learn that exceedingly high values, $L_{\text{FIR}}/M_{\text{gas}} \sim 10^4 L_{\odot} M_{\odot}^{-1}$, are found in a small region around the BN/KL core with $T_d \approx 95$ K. The global $L_{\text{FIR}}/M_{\text{gas}}$ ratio for M42 amounts to $14 L_{\odot} M_{\odot}^{-1}$, while in M43 it is $26 L_{\odot} M_{\odot}^{-1}$, and $7 L_{\odot} M_{\odot}^{-1}$ in NGC 1977. Thus, globally, the Orion Nebula is characterized by rather low $L_{\text{FIR}}/M_{\text{gas}}$ and probably not representative of environments that dominate the FIR emission in ULIRGs, that may comprise large amounts of embedded star-forming cores like BN/KL. As we will discuss below, those embedded sources show a FIR excess in the continuum emission compared to the line emission.

In conclusion, in particular dense H II regions (like the Huygens Region and M43) exhibit high $L_{\text{FIR}}/M_{\text{gas}}$ ratios in their centers. $L_{\text{FIR}}/M_{\text{gas}}$ is expected to be proportional to the H II ionization parameter $U = Q(H)/\pi R^2 c/n_e$ (Abel et al. 2009). Indeed, U is similar in M43 and NGC 1977 ($U \lesssim 10^{-5}$), but higher in the Huygens Region ($U \approx 10^{-2}$). The $L_{\text{FIR}}/M_{\text{gas}}$ ratio in Orion is dominated by the FIR emission from the dust column of the limb-brightened edges and the background molecular cloud (in M42 and M43) or the enveloping expanding shell (in NGC 1977) and does not trace the ionized gas directly. Yet, the properties of a PDR are closely related to the properties of the central H II region (Young Owl et al. 2002; Abel et al. 2005; Seo et al. 2019) and discussed further in Paper II.

We now turn to discuss the [C II] line deficit in spatially resolved samples, Orion A and M51. Figure 2 of Pineda et al. (2018) shows the [C II]/TIR versus TIR correlation and the [C II]/TIR versus 70 $\mu$m/160 $\mu$m correlation in the spiral galaxy M51 (with a spatial resolution of 0.6$''$ corresponding to 660 pc). Following Pineda et al. (2018), we compute the total infrared (TIR, integrated between 3 and 1000 $\mu$m; Croxall et al. 2012) intensity by

$$I_{\text{TIR}} = 0.95 I_{\nu,8\mu m} + 1.15 \nu I_{\nu,24\mu m} + \nu I_{\nu,70\mu m} + \nu I_{\nu,160\mu m}.$$  

(4)

Since the MIPS 24 $\mu$m image is saturated towards OMC1, we approximate $I_{\nu,24\mu m} \approx 0.12 I_{\nu,70\mu m}$, which is valid for most of the bright, edge-on structures in the Orion Nebula (see Paper II). With this, we find $I_{\text{TIR}}/I_{\text{FIR}} \sim 2$ towards the Orion Nebula. As extragalactic observations of regions of massive star formation are generally beam diluted, it is better to compare the relation between the [C II]/FIR and the 70 $\mu$m-160 $\mu$m color temperature. This latter ratio is a measure for the dust temperature. We show both correlations in Fig. 7 where for Orion we plot only points associated with M42 and M43. Points in NGC 1977 follow the same trend, but cover only the low-TIR end of the correlation. The trend of Pineda et al. (2018) is very similar to the trend observed in the Orion Nebula complex. The M51 relationship is slightly offset from the Orion data to lower 70 $\mu$m/160 $\mu$m ratios and/or lower [C II]/FIR. We ascribe this to a contribution of diffuse neutral HI clouds in the interstellar medium of M51 which is characterized by cooler dust.

In Orion, the [C II]/FIR ratio drops particularly for regions that are close to the illuminating star. These are regions with $G_0 > 10^4$ and $n > 4 \times 10^4$ cm$^{-3}$. For these regions cooling by $[O I] 63\mu m$ is known to be important with $I_{[O I] 63\mu m}/I_{\text{C II} 158\mu m} \approx 5-10$ (Herrmann et al. 1997). Following Luhman et al. (2003) and Croxall et al. (2012), we attribute the drop in the [C II]/FIR relation with increasing FIR or 70 $\mu$m color temperature to a shift of the gas cooling to $[O I] 63\mu m$ line. Implicitly, this implies that the heating efficiency does not depend strongly on the physical conditions in the emitting region. Variations in the heating efficiency are generally ascribed to variations in the ionization balance, which is controlled by the PDR ionization parameter $\gamma = G_0 T^{1/2}/n_e$ (cf. Section 1.3 Bakes & Tielens 1994). The observed relation between $G_0$ and the thermal pressure $p_{\text{th}} = n_k T$ (see Paper II) translates this into a very weak dependence of the ionization parameter on physical conditions. We note that the [C II] optical depth of the bright [C II]-emitting structures in Orion A is usually of the order $\tau_{[\text{C II}] - 1-3}$, both in the edge-on shells and in the very bright core OMC1 (see Paper II; Goicoechea et al. 2015b), which may affect the correlations slightly, but we deem the effect too small to correct for the [C II] deficit. When estimating star-formation rates of galaxies, however, the [C II] optical depth has to be taken into account, as Okada et al. (2019) point out.

Besides close to the central heating sources, where $[O I]$ cooling is dominant, low [C II]/FIR ratios ($I_{[\text{C II}]}/I_{\text{FIR}} \sim 2 \times 10^{-3}$) are found along the dense spine of the ISF (cf. Fig. 21). Considering the low temperature of these structures,
we do not expect [O\textsc{i}] emission to contribute significantly. Rather, we interpret these ratios as a “FIR excess” from cold dust in the dense molecular gas. Particularly deficient [C\textsc{ii}]/FIR ratios ($I_{[C\textsc{ii}]}/I_{\text{FIR}} \simeq 2 \times 10^{-3}$) are also found towards the active star-forming cores in the BN/KL region and Orion S (FIR intensity from Goicoechea et al. 2015a). Here, [O\textsc{i}] cooling is dominant ($I_{[O\textsc{i}]}^{63\mu m}/I_{[C\textsc{ii}]}^{158\mu m} \simeq 20$ Herrmann et al. 1997), but in addition to excitation by FUV radiation at the surface, the [O\textsc{i}] lines have a contribution from shocked gas in the interior (Goicoechea et al. 2015a). Also the FIR emission stems from the inner layers of embedded star formation. As opposed to the FIR excess from cold dust in the ISF, this FIR excess is produced by warm molecular gas in the star-forming cores. The heavily irradiated PDR on the surface of the molecular core east of the Trapezium stars, devoid of star-forming activity, shows less deficient FIR line ratios, ($I_{[C\textsc{ii}]} + I_{[O\textsc{i}]})/I_{\text{FIR}} \simeq 5-10 \times 10^{-3}$.

Large columns of warm dust, such as in BN/KL and Orion S, lead automatically to high $L_{\text{FIR}}/M_{\text{gas}}$ ratios, as we have shown by Eq. 2, whereas the effective dust temperature will be lower for an irradiated surface with a large column of cooler (not internally heated) material behind it. Fig. 8 shows that the [C\textsc{ii}]/FIR ratio in Orion A decreases with increasing $L_{\text{FIR}}/M_{\text{gas}}$ ratio for $L_{\text{FIR}}/M_{\text{gas}} \gtrsim 5$. At lower $L_{\text{FIR}}/M_{\text{gas}}$ ratios, however, the [C\textsc{ii}]/FIR ratio tends to increase with increasing $L_{\text{FIR}}/M_{\text{gas}}$.

In Section 7.2 we have shown that the [C\textsc{ii}] luminosity depends less than linear on the FIR luminosity per pixel. While the regions we study have different stellar content, the [C\textsc{ii}]-FIR correlation is very similar in all of the regions. Moreover, we note that the [C\textsc{ii}]/FIR versus FIR in the L1630 region (Pabst et al. 2017) is a good continuation of the correlation in the central OMC1 (Goicoechea et al. 2015b). Yet, L1630 represents the chance encounter of an O star with a molecular cloud (Ochsendorf et al. 2014) rather than emission from a region of active massive star formation. This provides further support for an interpretation of the [C\textsc{ii}]/FIR relation in terms of the physical conditions rather than the star-formation history of the region. On the other hand, we have argued that particularly low FIR line-to-continuum ratios are found towards regions of large columns of (warm and cold) dust, which suggests the interpretation of the FIR line “deficit” in terms of a “FIR excess”.

4.3. The photoelectric heating efficiency

The heating mechanism of the interstellar gas is of great importance for the understanding of the properties of the ISM. The UV-illuminated gas is dominantly heated by the photoelectric effect acting on small grains and PAHs (Bakes & Tielens 1994; Wolfire et al. 1995). The efficiency of this process is a crucial parameter in models of the ISM. Assuming equilibrium of heating and cooling processes, we can estimate the photoelectric heating efficiency by the cooling efficiency of the gas. At intermediate temperatures and densities the cooling is dominated by cooling through the [C\textsc{ii}] line. At higher temperatures and densities, like those in the Huygens Region, the [O\textsc{i}] $63 \mu m$ line becomes important (Hollenbach & Tielens 1999). However, in the shell surrounding the Extended Orion Nebula, gas cooling is most
likely dominated by [C\textsc{ii}], as the temperatures and densities are rather moderate. In M43, [O\textsc{ii}] 63\mu m emission will be important, in NGC 1977 only in the densest part of the shell abutting OMC3 (Herrmann et al. 1997; Young Owl et al. 2002).

Theoretically, the photoelectric heating efficiency depends on the ionization parameter \(\gamma = G_0 T^3/n_e\) (Bakes & Tielens 1994, Eq. 43). We equate the heating efficiency in our sample with the [C\textsc{ii}] cooling efficiency \(I_{[\text{C\textsc{ii}}]}/I_{\text{FIR}}\), which is accurate for most points in our data set. In App. A we estimate \(\gamma\) in each pixel of the map. The correlation between the photoelectric heating efficiency \(\epsilon\) and the ionization parameter \(\gamma\) in the Orion Nebula is shown in Fig. 9. Points in NGC 1977 overlap and are not shown. The data reveal a similar trend with a decreased efficiency with increased ionization parameter as the theoretical predictions of Bakes & Tielens (1994). The offset between the two might reflect a somewhat lower abundance of PAHs and VSGs in Orion than assumed by Bakes & Tielens (1994). Closer to the central source, [O\textsc{i}] cooling dominates. Adding the [O\textsc{ii}] 63\mu m intensity to the [C\textsc{ii}] intensity, shifts the heating/cooling efficiency to \(\epsilon \approx 7 \times 10^{-3}\) (outside of BN/KL) and corrects for the steep decline in the [C\textsc{ii}]-TIR plot (with \(I_{[\text{O\textsc{i}}]}/I_{[\text{C\textsc{ii}}]} \approx 6\) in OMC1). Nevertheless, the heating efficiency seems to slightly decline with radiation field, from \(\sim 10^{-2}\) in the distant shell to \(5 \times 10^{-3}\) in the very center. While the [C\textsc{ii}] deficit (and other FIR line deficits) observed on galactic scales might reflect different physical processes (XDRs, AGN activity), the [C\textsc{ii}] deficit in the Orion Nebula reflects PDR physics with [O\textsc{i}] cooling correcting for the majority of the [C\textsc{ii}] deficit and a slightly decreased heating efficiency at higher radiation field causing the slight decline.

4.4. The origin of [C\textsc{ii}] emission

Table 3 gives the luminosities and masses of M42, M43, and NGC 1977, total and for the respective brightest region and the extended shell structure. Paper II discusses the origin of the [C\textsc{ii}] emission in greater detail.

Most of the [C\textsc{ii}] emission stems from the limb-brightened shell edges in M42, M43, and NGC 1977 (30-50\%), but a significant contribution also comes from the diffuse emission (25-45\%), that is faint emission from extended surfaces. Even though the regions close to the central stars are very bright, their area is small and the contribution to the total [C\textsc{ii}] emission minor (10-20\%) compared to the large shells. For FIR emission, 20-30\% stem from the shells, 20-30\% from the regions close to the central stars of M43 and NGC 1977, but 45\% from OMC1 in M42, and 10-20\% from diffuse emission.

In Galactic samples, Pineda et al. (2013) note that most of the [C\textsc{ii}] emission arises in moderately FUV-illuminated regions \((G_0 \approx 2-50\) in Habing units), that is large faint surfaces rather than small extreme regions. Our observations towards the Orion Nebula are reminiscent of this, the bright inner OMC1 region being a minor contributor to the total [C\textsc{ii}] luminosity. The [C\textsc{ii}] observations towards L1630, comprising the Horsehead Nebula, predominantly highlight the PDR surfaces illuminated by \(\sigma\) Ori, where 95\% of the total [C\textsc{ii}] emission in the mapped area arise. Yet, regions that are bright in [C\textsc{ii}] trace only 8\% of the gas mass, while 85\% of the mass is associated with strong CO emission (Pabst et al. 2017). In the Orion Nebula complex, we find that 70\% of the [C\textsc{ii}] emission arises in bright PDR surfaces with \(G_0 > 100\). The [C\textsc{ii}]-emitting regions contain 64\% of the gas mass (traced by dust). A portion of that gas mass, about 30-50\%, is likely associated with the molecular background rather than the PDR surface. Hence, bright [C\textsc{ii}] emission, that traces the H2 transition in a PDR, traces about 30\% of the total gas mass in the Orion Nebula complex.

We conclude that [C\textsc{ii}] emission from PDRs with \(G_0 \gtrsim 100\) is the main origin of [C\textsc{ii}] emission from the Orion Nebula complex, with about 70\%. The [C\textsc{ii}] emission from ionized gas is a minor contributor, less than 5\% in M42 and NGC 1977, but 15\% in M43. From the remainder, we
Table 3. Luminosities and masses of M42, M43, and NGC 1977.

| Region  | $A$ [pc$^2$] | $L_{\text{FIR}}$ [$L_\odot$] | $L_{\text{[C}\text{II]}}$ [$L_\odot$] | $M_{\text{gas}}$ [$M_\odot$] | $L_{\text{CO}(2-1)}$ [$L_\odot$] | $M_{\text{CO}}$ [$M_\odot$] | $L_{24\mu\text{m}}$ [$L_\odot$] | $L_{\text{H}\alpha}$ [$L_\odot$] |
|---------|-------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| M42     | all         | 45 1.8 × 10$^7$            | 510 2.8 × 10$^-3$           | 10 000 1.1                 | 8 800 4700                  | 3 500                      |
|         | OMC1        | 0.4 8.2 × 10$^-4$           | 53 6.5 × 10$^-4$            | 640 8.9 × 10$^-2$          | 720 − 1500                 |
|         | shell       | 10.0 5.2 × 10$^4$           | 209 4.0 × 10$^-3$           | 3 000 3.2 × 10$^-1$        | 2 500 2 000                  | 850                     |
| M43     | all         | 0.74 1.4 × 10$^6$           | 38 2.7 × 10$^-3$            | 530 3.0 × 10$^-2$          | 240 740                     | 190                     |
|         | background, H$\text{II}$ | 0.13 3.1 × 10$^8$       | 8.9f 2.8 × 10$^-3$          | 53 4.6 × 10$^-3$           | 37 100                     | 99                     |
|         | shell       | 0.31 8.2 × 10$^5$           | 19 2.3 × 10$^-3$            | 250 1.4 × 10$^-2$          | 110 410                     | 63                     |
| NGC 1977| all         | 17 1.8 × 10$^4$            | 160 8.9 × 10$^-3$           | 2 600 1.2 × 10$^-1$        | 950 1 000                   | 1 063                  |
|         | OMC3        | 2.6 5.8 × 10$^5$           | 34 5.9 × 10$^-3$            | 1 200 8.9 × 10$^-2$        | 720 190                     | 8.6                    |
|         | shell       | 6.2 5.4 × 10$^4$           | 69 1.3 × 10$^-2$            | 670 1.6 × 10$^-2$          | 130 100                     | 7.9                    |

Notes. (a) Gas mass derived from dust mass, using $N_H \simeq 6 \times 10^{24} \text{cm}^{-2} \tau_{100}$ (Weingartner & Draine 2001). (b) The CO(2-1) map does not cover the entire NGC 1977 region (cf. Fig. 2). (c) Molecular gas mass from CO(2-1) intensity, using $X(\text{CO}) \simeq 2 \times 10^{20} \text{cm}^{-2} (\text{K km s}^{-1})^{-1}$ (Bolatto et al. 2013). (d) The MIPS 24$\mu$m image is saturated towards the Huygens/OMC1 region. (e) The H$\alpha$ surface brightness in the EON is largely due to scattered light from the bright Huygens Region (O’Dell & Harris 2010). Also H$\alpha$ emission in M43 has to be corrected for a contribution of scattered light from the Huygens Region (Simón-Díaz et al. 2011). (f) BN/KL and Orion S contribute with $L_{\text{FIR}} \simeq 3 \times 10^8 L_\odot$.

Fig. 10. SFR surface density, estimated from H$\alpha$ and 24$\mu$m emission (Calzetti et al. 2007) versus the [C$\text{II}$] luminosity per unit area in Orion A as point-density plot. The grey line indicates the relation calibrated by Herrera-Camus et al. (2015) from a sample of local galaxies. Estimate that less irradiated gas that is not captured in bright PDR surfaces, contributes with about 20% within the mapped area. These percentages elucidate the importance of observations towards fainter extended regions, for those can carry a significant amount of [C$\text{II}$] luminosity (Abdullah & Tielens 2020).

4.5. Tracers of the star-formation rate

Observations with COBE revealed that the [C$\text{II}$] line is the brightest emission line in the far-IR spectrum of the Milky Way (Bennett et al. 1994). As this line originates from gas illuminated by FUV photons emitted by OB stars, it was quickly recognized that this line might provide an excellent probe of the star formation rate in distant galaxies. Indeed, one of the main drivers of the design of ALMA was the requirement to be able to detect this line in Milky Way type galaxies at redshifts of $z \sim 3$. Since then, various Herschel-based studies have calibrated the [C$\text{II}$] line as a star-formation rate indicator. We discuss the relations compiled in Table 3 in the context of our observations towards...
the Orion Nebula complex. Table 5 summarizes the values we calculate with these formulae for the star-formation rate from observations, both total and divided into the three regions M42, M43 and NGC 1977.

Perusing Table 5 we conclude that the different tracers of star-formation predict significantly different values at our mapped spatial scales. Specifically, the two SFR estimates from the [C ii] luminosity differ from each other by an order of magnitude. Overall, the relation derived by Herrera-Camus et al. (2015) predicts lower values than expected from other traces such as FIR, Hα and 24 µm emission. Only in NGC 1977, the relation by Pineda et al. (2014) overpredicts the SFR compared to the other traces (besides CO-traced mass).

In general, our correlations show that the [C ii] intensity depends not linearly on the FIR intensity, but by a power law: it increases less steeply than the FIR intensity (Sec. 4.1). This reflects the decreased heating efficiency at higher radiation field (Sec. 4.3). This means that the galactic relations of FIR and [C ii] emission are compatible with each other only within a limited range of conditions. The predictive power of the [C ii] line in galactic context depends on the dominant source of [C ii] line emission. A study by Abdullah & Tielens (2020) of the Orion-Eridanus environment on ~ 400 pc scale suggests that [C ii] emission arises mostly from extended, moderately irradiated cloud surfaces.

We note that the different measures for the star-formation rate trace different evolutionary stages in the star-formation process. While the dense mass mainly traces the sites of potential future star formation, Hα traces visible sites of already existing massive stars, that are ionizing their environment. The FIR luminosity also includes contributions from the embedded phase of massive star formation which is missed by Hα and 24 µm. For galactic sources, this phase is rather short and gets averaged out in the beam, but that is not always the case in extragalactic settings (e.g., ULIRGs with vigorous embedded star formation). Moreover, locally the 24 µm intensity, tracing the warmer shell interiors, is not correlated with the [C ii], FIR and 8 µm intensities, that trace the somewhat cooler gas in PDR surfaces. Locally, also the ionized gas emitting in Hα fills the space interior to the shells.

We compare the gas-derived SFR with an actual count of the YSOs in the Orion Nebula cluster (ONC). Megeath et al. (2016) report 3001 YSOs in the ONC (after sample incompleteness correction). Adopting an average mass of 0.5 M⊙ and an average duration of the protostellar/disk phase of 2 Myr (Evans et al. 2009), gives an SFR of 7.5 × 10⁻³ M⊙ yr⁻¹. De Buizer et al. (2014) estimate a total mass of the ONC of 1000 M⊙. Using the age of the cluster of 2 Myr, this yields a SFR of 5 × 10⁻³ M⊙ yr⁻¹. Not surprisingly, as we are zooming in on a region of active star formation, these values are significantly higher than suggested by extragalactic correlations. This is illustrated by comparing the results in Table 5 with the upper-left panel of Figure 1 in Pineda et al. (2015), the SFR-[C ii] correlation per unit surface. The Orion Nebula complex lies off the upper right end of the correlation, with log Σ_{Cii}[erg s⁻¹ kpc⁻²] ≃ 40.7 and log Σ_{SFR}[M⊙ yr⁻¹ kpc⁻²] ≃ 0.9-1.7 from star and YSO counts or log Σ_{SFR} ≃ 0.1 from Hα and 24 µm emission. We note, however, that a pixel-by-pixel comparison of the SFR predicted by Hα and 24 µm emission (according to Calzetti et al. 2007) and the [C ii] emission in the Orion Nebula, as shown in Fig. 10, exhibits a similar spread as the SFR-[C ii] correlation of Pineda et al. (2018) (here, p ≃ 0.78 and rms ≃ 0.45 dex), despite the fact that the emission tracers possess different morphologies. In the Orion Nebula, the Hα and 24 µm emission are strong in the (ionized) shell interior, whereas [C ii] emission is arising predominantly from the shell’s PDR surfaces.

Zooming into separate regions, we discuss the distribution of the YSOs, as catalogued by Megeath et al. (2012), in relation with [C ii] emission in somewhat more detail. Fig. 11 shows the distributions of YSOs across the [C ii]-mapped area. We have counted the YSOs per 14” pixel and convolved the resulting surface density to a beam of 2’. At our spatial resolution, the [C ii] intensity is not correlated with the YSO surface density locally, which also means a lack of evidence for triggered star formation in this early stage of evolution of the expanding shells in the Orion Nebula complex (see also Goicoechea et al. 2020). Strikingly, while OMC2 does not exhibit bright [C ii] emission, we find many YSOs (about 120 within 1.6 pc²) located in the line of sight towards OMC2, concentrated along the ISF. Towards NGC 1977, we find about 300 YSOs across 17 pc². The majority of YSOs is located in front of M42 and M43, about 1100 YSOs distributed over 42 pc². Here, the YSO surface density is 26 M⊙ pc⁻², where we have used an average mass of 0.5 M⊙ and corrected for sample incompleteness by a factor of 2, following Megeath et al. (2016). The YSO surface density is slightly lower in NGC 1977, 18 M⊙ pc⁻², but highest of the three regions in OMC2 with 75 M⊙ pc⁻². Generally, high YSO surface density is found along the ISF, concentrating in the molecular cores OMC1–4. The maximum surface density is found towards OMC1. Thus, the SFR is highest in M42 and M43, together 6 × 10⁻⁴ M⊙ yr⁻¹. NGC 1977 and OMC2 count with 2 × 10⁻⁴ M⊙ yr⁻¹ and 6 × 10⁻⁵ M⊙ yr⁻¹, respectively. We note that the removal of some 40% of the mass from the OMC1 core by the stellar wind of θ¹ Ori C will decrease the gravitational binding of the ONC cluster. We expect that it will take some 10⁸ years for the stars to respond.

From COBE observations, Abdullah & Tielens (2020) derive a [C ii] flux of 6.9 × 10⁻¹ erg s⁻¹ cm⁻² from a region encompassing the Orion Nebula and NGC 1977. This corresponds to 3.7 × 10³ L⊙. Hence, the SFR relations of Pineda et al. (2014) and Herrera-Camus et al. (2015) predict 6 × 10⁻⁴ M⊙ yr⁻¹ and 6 × 10⁻⁵ M⊙ yr⁻¹, respectively. Taking into account the contribution of molecular cloud surfaces exposed to only moderate radiation fields, averaged in the beam of COBE, thus increases the SFR derived from extragalactic correlations. Locally, the SFR can be much higher (like in the Orion Nebula), but on galactic scales larger structures may contribute significantly, as we noted that a large portion of the [C ii] luminosity from the Orion Nebula complex stems from rather extended, low-intensity regions (cf. Section 4.4).

5. Conclusion

Using a square-degree sized map of the [C ii] 158 µm line towards the Orion Nebula complex, including M43 and NGC 1977, obtained with SOFIA/upGREAT, and com-

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6 Since these are empirical relations, we do not correct for [C ii] optical depth.

7 The total [C ii] luminosity from the Orion Nebula complex is 750 L⊙ from an area of 62 pc².
paring with Herschel/PACS and SPIRE FIR photometry. Spitzer/IRAC 8 µm emission and velocity-resolved IRAM 30m CO(2-1) observations, we have obtained the following results:

1. Our comparison of the [CII] line emission with FIR emission from FUV-heated dust and PAH emission in the 8 µm band reveal tight correlations with correlation coefficients of $\rho \gtrsim 0.9$. The [CII] line-integrated intensity depends less than linear on the PACS 70 µm intensity, FIR (40-500 µm) intensity, and IRAC 8 µm intensity. In particular, we find that the [CII] intensity scales with the 70 µm, FIR intensity, and the 8 µm intensity to the power of $\sim 0.6$ each. The FIR and PAH 8 µm intensities are approximately linearly correlated, the IRAC 8 µm band carrying about 10% of the FIR emission.

2. The less-than-linear dependence of the [CII] intensity on the FIR intensity implies a decreasing [CII]/FIR ratio with increasing FIR intensity. This is reminiscent of the “[CII] deficit” in ULIRGs, that has also been observed towards extragalactic sources like M51. However, including [OIII] cooling corrects for most of the deficit in the Orion Nebula complex. The remaining slight deficit can be attributed to a reduced heating efficiency in the heavily irradiated PDR surfaces close to the central stars. Some sight lines host large columns of (warm and cold) dust that produce a “FIR excess”, leading to particularly low [CII]/FIR intensity ratios.

3. Most of the [CII] luminosity of the Orion Nebula complex, 33% of the total 750 $L_\odot$, arises in the large, moderately illuminated shells surrounding the Orion Nebula, M43, and NGC 1977. Only 10% of the [CII] luminosity in M42, 53 $L_\odot$, stem from the brightest region, OMC1. A large amount of [CII] luminosity, 35%, stems from extended faint surfaces.

4. The scaling relations invoked to estimate the star-formation rate on galactic scales and in high-redshift galaxies do not apply to our local sample of [CII]-emitting sources. In the Orion Nebula complex, the [CII] line is dominantly excited by FUV radiation from the most massive stars. Smaller sources contribute to small-scale [CII]-emitting structures but minor to the large-scale shells surrounding the massive stars. However, even the total [CII] emission from the mapped area is short of predicting the YSO content within the field of view. We surmise that [CII] emission from extended [CII]-faint structures contribute significantly to [CII] emission on galactic scales. In our sample, [CII] emission is dominated by larger, comparatively faint structures, rather than the bright dense cores.

Studies of the relations of [CII] emission to other tracers of gas and dust held to reveal “the local truth” about the origins of the [CII] line emission. Further investigations have to show whether the same correlations between those gas and dust tracers hold in different environments, for instance, the starburst region 30 Doradus (with also lower metallicity) and other sources shaped by stellar feedback. Taking into account the geometry of the sources is crucial in understanding the details of the correlations.

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### Table 4. Star-formation rates from different tracers

| Tracer | SFR($M_\odot$ yr$^{-1}$) | Reference |
|--------|--------------------------|-----------|
| FIR    | 4.5 × 10$^{-44}$ L(FIR) (erg s$^{-1}$) | Kennicutt (1998) |
| Hα, 24 µm | 5.3 × 10$^{-42}$ (L(Hα)_{obs} + 0.0031 L(24µm)) (erg s$^{-1}$) | Calzetti et al. (2007) |
| 24 µm | 1.27 × 10$^{-38}$ [L(24µm)] (erg s$^{-1}$)$^{0.8850}$ | Calzetti et al. (2007) |
| Hα, TIR | 5.5 × 10$^{-42}$ [L(Hα)_{obs} + 0.0024 L(TIR)] (erg s$^{-1}$) | Kennicutt et al. (2009) |
| [CII](1) | 5.0 × 10$^{-37}$ [L([CII]) (erg s$^{-1}$)]$^{0.89}$ | Pineda et al. (2014) |
| [CII](2) | 2.286 × 10$^{-43}$ [L([CII]) (erg s$^{-1}$)]$^{1.034}$ | Herrera-Camus et al. (2015) |
| dense gas | 1.5 × 10$^{-8}$ $M_{\text{dense}} (M_\odot)$ | Lada et al. (2012) |

### Table 5. Star-formation rates in $M_\odot$ yr$^{-1}$ in M42, M43 and NGC 1977 predicted by several tracers using the correlations presented in Table 4

| Region  | FIR | Hα, 24 µm | 24 µm | Hα, TIR$^a$ | [CII](1) | [CII](2) | dense gas$^b$ | YSOs |
|---------|-----|-----------|-------|-------------|---------|---------|-------------|------|
| all     | 3.0 × 10$^{-5}$ | 7.7 × 10$^{-5}$ | 1.6 × 10$^{-5}$ | 1.0 × 10$^{-4}$ | 1.3 × 10$^{-4}$ | 1.1 × 10$^{-5}$ | 1.5 × 10$^{-4}$ | 7.5 × 10$^{-4}$ |
| M42     | 2.4 × 10$^{-5}$ | 7.1 × 10$^{-5}$ | 1.2 × 10$^{-5}$ | 9.2 × 10$^{-5}$ | 9.9 × 10$^{-5}$ | 7.6 × 10$^{-6}$ | 1.3 × 10$^{-4}$ | 5.5 × 10$^{-4}$ |
| M43     | 2.4 × 10$^{-6}$ | 3.9 × 10$^{-6}$ | 2.3 × 10$^{-6}$ | 5.4 × 10$^{-6}$ | 9.9 × 10$^{-6}$ | 5.2 × 10$^{-7}$ | 3.6 × 10$^{-6}$ | – |
| NGC 1977| 3.1 × 10$^{-6}$ | 1.3 × 10$^{-6}$ | 3.0 × 10$^{-6}$ | 3.1 × 10$^{-6}$ | 3.5 × 10$^{-5}$ | 2.3 × 10$^{-6}$ | 1.4 × 10$^{-5}$ | 1.5 × 10$^{-4}$ |

Notes. (a) Total infrared luminosity approximated by twice the far-infrared luminosity. (b) Dense gas taken as CO-traced mass.
Appendix A: Calculation of the ionization parameter $\gamma$

We use the ionization parameter $\gamma = G_0 T_{\text{gas}}^{1/2}/n_e$ in Section 4.3 to semi-empirically determine the heating curve of the interstellar gas. Here, we elaborate the procedure by which we estimate $\gamma$ throughout the [C II] map.

To obtain the kinetic temperature of the gas we use the peak temperature $T_P$ of the [C II] line:

$$T_{\text{gas}} = \frac{T_{\text{ex}}}{1 - T_{\text{ex}}/91.2 \text{ K} \log(1 + n_{\text{cr}}/n)}$$

(A.1)

where the critical density depends on the [C II] optical depth $\tau_{\text{[C II]}}$, $n_{\text{cr}} = n_{\text{cr,0}} \beta(\tau_{\text{[C II]}})$, and $n_{\text{cr,0}} = 2.7 \times 10^3 \text{ cm}^{-3}$. The function $\beta(\tau)$ can be approximated as $(1 - \exp \tau)/\tau$. For simplicity, we fix $\tau_{\text{[C II]}} = 2$, as is consistent with the $[^{13}\text{C II}]$ line analysis where possible (see Paper II). We note that the gas temperature is only weakly dependent on the exact value of $\tau_{\text{[C II]}}$. We estimate the excitation temperature $T_{\text{ex}}$ assuming optically thick emission:

$$T_{\text{ex}} = \frac{91.2 \text{ K}}{\log(91.2 \text{ K}/(T_P + J(T_\lambda)) + 1)}$$

(A.2)

We approximate the gas density by the gas column density estimated from the dust opacity, assuming a line of sight of $\sim r/2 \simeq 1.4 \text{ pc}$, i.e. $n \sim 6 \times 10^{23} \text{ cm}^{-2} \tau_{160}/1.4 \text{ pc}$ in the Veil shell; in the OMC1 region, we take $n \sim 10^5 \text{ cm}^{-2}$, in accordance with studies of the Orion Bar (Pellegrini et al. 2009; Bernard-Salas et al. 2012; Goicoechea et al. 2015b). We assume that all electrons stem from carbon ionization and that carbon is fully ionized. For the radiation field in the Orion Nebula, we assume $G_0 \simeq 500(1 \text{ pc}/(d + 0.1 \text{ pc}))^2$, as obtained from the FIR-d relation in Section 3.2. We note that for points close to $\theta^1$ Ori C, the estimate of the radiation field using the projected distance is not accurate and we add the vertical offset of 0.1 pc.