The Metallicity Distribution Function in Outer Halo Fields of Simulated Elliptical
Galaxies Compared to Observations of NGC 5128

Ena Choi1 ©, Jeremiah P. Ostriker2,3 ©, Michaela Hirschmann4,5,6 ©, Rachel S. Somerville7, and Thorsten Naab8 ©
1 Quantum Universe Center, Korea Institute for Advanced Study, 85 Hoegiro, Dongdaemun-gu, Seoul 02455, Republic of Korea; enachoi@kias.re.kr
2 Department of Astronomy, Columbia University, 550 West 120th Street, New York, NY 10027, USA
3 Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544, USA
4 Institut de Physique, Laboratoire d’astrophysique, École Polytechnique Fédérale de Lausanne (EPFL), CH-1290 Versoix, Switzerland
5 INAF–Osservatorio Astronomico di Trieste, via G.B. Tiepolo 11, I-34143 Trieste, Italy
6 DARK, Niels Bohr Institute, University of Copenhagen, Lyngbyvej 2, DK-2100 Copenhagen, Denmark
7 Center for Computational Astrophysics, Flatiron Institute, 162 5th Avenue, New York, NY 10010, USA
8 Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Strasse 1, D-85741 Garching, Germany

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Abstract
Stellar metallicity distribution functions (MDFs) have been measured for resolved stellar populations in the outer halos of many galaxies in nearby groups. Among them, the MDF of NGC 5128, the central giant elliptical in the Centaurus group, provides essential constraints for theories of massive galaxy formation and hierarchical assembly. To investigate the formation and chemical evolution history of the outer halo of giant elliptical galaxies, we examine the chemical properties of three zoom-in high-resolution cosmological hydrodynamical simulations of an NGC 5128–like giant elliptical galaxy and compare their outer halo MDFs to the observed one of NGC 5128. Even though the simulated galaxies have different merging histories and age distributions, all predicted MDFs are in good qualitative agreement with the observed one. The median metallicity of the simulated galaxies is, on average, $[M/H] = -0.41 \pm 0.06$ compared to the observed value of $[M/H] = -0.38 \pm 0.02$ for NGC 5128, and the dispersion in metallicity is $\sim 0.77$ dex for both observed and simulated galaxies. We investigate the origin of the stars ending up in the outer halo field of simulated galaxies and show that most have an “accreted” origin, formed in other small galaxies and later accreted in mergers. Only $\sim 15\%$ of the stars are formed in situ within the main progenitor of the galaxy and radially migrate outward. We show that the contribution of metal-rich in situ stars is subdominant in the outer halos of our simulated galaxies but can be prominent in the inner regions.

1. Introduction
Metallcity distribution functions (MDFs) have long been used to inform chemical evolution models, as they provide constraints on the star formation history of a galaxy and the merging history of its progenitors (e.g., Tinsley 1980; Pagel 1989). The MDF has only been well characterized observationally in the solar neighborhood (van den Bergh 1962). However, starting with the pioneering spectroscopic study of stars in Baade’s window (Rich 1988), the estimates of the MDF in several fields in the Milky Way have provided unique opportunities to understand the complex formation history of the Galaxy (e.g., Zoccali et al. 2008; Hill et al. 2011; Zoccali et al. 2017). Recently, the Apache Point Observatory Galactic Evolution Experiment survey provided MDFs across an unprecedented volume of the Milky Way, allowing a comprehensive characterization of the chemical history of the galaxy (Anders et al. 2014; Hayden et al. 2015; Rojas-Arriagada et al. 2020). These observed MDFs have been compared to predicted MDFs from cosmological hydrodynamical simulations and semianalytic models of the Galaxy and provided vital new insights into the formation histories of the Galaxy (Calura et al. 2012; Toyouchi & Chiba 2018; Mackereth et al. 2019).

For external galaxies, the study of the MDF is limited to galaxies in the Local Group and nearby groups. The MDFs can be measured by analyzing the color distribution of stars on the red giant branch (RGBs; e.g., Harris et al. 1999). Deep imaging by the Hubble Space Telescope (HST) allows us to perform accurate stellar photometry in very crowded fields and has provided large photometric samples of individual RGB stars in nearby galaxies (e.g., Helmi et al. 2006; Harris et al. 2007a, 2007b; Durrell et al. 2010; Mould & Spitler 2010; Monachesi et al. 2016; Cohen et al. 2020). This opened up new windows into galaxy formation and assembly. By using the observed MDFs of RGB stars as a constraint, detailed models of chemical evolution have been developed and applied to Local Group galaxies (Calura & Menci 2009; Tsujimoto 2011; Romano & Starkenburg 2013; Homma et al. 2015). The predicted MDFs from cosmological hydrodynamical simulations have been analyzed and intensively compared to those observed for dwarf galaxies (Pilkington et al. 2012; Escala et al. 2018), Milky Way–like disk galaxies (Calura et al. 2012), and ultrafaint dwarfs (Jeon et al. 2017).

However, there have been few if any studies of the MDFs of massive elliptical galaxies formed in high-resolution cosmological simulations that would enable a comparison to current observations (see Bekki et al. 2002, for noncosmological simulations). This may be partly due to the limited number of observed MDFs for resolved stars in elliptical galaxies, as
resolved stellar photometry can only be applied to a small number of nearby systems.

Among them, NGC 5128, also known as Centaurus A, located at a distance of ~3.8 Mpc (Hui et al. 1993; Harris et al. 2010), is currently the only viable target for wide-field resolved stellar population analysis of a giant elliptical (gE) galaxy. It is the dominant galaxy in the Cen A group and the closest gE galaxy in the nearby universe (van den Bergh 1976). Despite its prominent dust lane along the photometric minor axis, the nature of its main elliptical component was well established via absorption lines and the surface brightness distribution (Israel 1998). Its old red giant stars in the outer halo can be studied with HST imaging (Soria et al. 1996; Harris et al. 1999) or a ground-based telescope under very good seeing conditions (Crnojević et al. 2013). As HST observations reach at least 1–1.5 mag below the RGB tip, resolved stars in several fields of the outer halo of NGC 5128 have been intensively investigated by many authors (Harris et al. 1999; Harris & Harris 2002; Rejkuba et al. 2005), reaching out to a projected radius of 140 kpc (Rejkuba et al. 2014). The outermost fields are usually poorly sampled because of small number statistics, but several inner target fields are well sampled. For example, the target field of Rejkuba et al. (2005) with a galactocentric distance of \( r_{gc} = 40 \) kpc in projection is well sampled with \( \sim 2900 \) stars. Rejkuba et al. (2005) found that the metallicity distribution of upper RGB stars in this outer halo field is moderately metal-rich and broad.

The observed MDF in the outskirts of a gE can provide a significant constraint on models of elliptical galaxy formation. For example, in the currently favored “two-phase formation” model of massive galaxies (e.g., Oser et al. 2010), intensive dissipational processes such as cold accretion (Dekel et al. 2009) or gas-rich major mergers form an initially compact inner component, and then the outer part grows by the repeated merging of smaller galaxies through nondissipational processes such as dry minor mergers (Naab et al. 2007; Oser et al. 2010; Naab & Ostriker 2017). As this buildup of the stellar envelope is dominated by the accretion of old stars from lower-mass galaxies, the model predicts that the outskirts of galaxies should be populated by stars with older ages and lower metallicities (Hirschmann et al. 2015), in contrast with other formation models, such as monolithic collapse (Eggen et al. 1962; Larson 1975) or binary major mergers (Toomre et al. 1972).

The properties of stars beyond the central regions of gE have mostly been explored with integrated light analyses due to the faintness of the outer regions (Coccato et al. 2010; Greene et al. 2012). Detailed information on the metallicity distribution of outer halo stars from the resolved stellar photometry can provide important constraints for massive galaxy formation. Comparing the observed distribution functions of metallicity and age to the predictions of cosmological simulations of massive galaxy formation would allow us to test the two-phase massive galaxy formation scenario and better understand the complex formation histories of massive galaxies.

In this paper, we qualitatively and quantitatively examine how the simulated galaxies compare with the latest observations of the MDF of the resolved stellar populations in the local elliptical galaxy NGC 5128 in a full cosmological context. We first focus on the metallicity distribution of stars in the outer halo field with a galactocentric radius of \( r_{gc} \approx 40 \) kpc, where we have well-sampled observational data from Rejkuba et al. (2005) for comparison. We also analyze the buildup of the simulated MDF, tracing the formation history of stars in the outer halo. We then study the variations in the MDF of simulated galaxies with radial distance.

2. Simulation and Method

2.1. Simulation

We use the suite of cosmological hydrodynamical simulations presented in Choi et al. (2017). In the following, we provide a brief summary of the simulations, and we refer the reader to Choi et al. (2017) for further details.

The cosmological zoom-in simulations of massive galaxies were generated with SPHGal (Hu et al. 2014), which is a modified version of the parallel smoothed particle hydrodynamics (SPH) code GADGET-3 (Springel 2005). It includes a number of improvements to overcome the classical numerical fluid-mixing problems of SPH codes, such as a density-independent pressure-entropy SPH formulation (Ritchie & Thomas 2001), an improved artificial viscosity (Cullen & Dehnen 2010), and an artificial thermal conductivity (Read & Hayfield 2012). The initial conditions of the zoom-in regions were adopted from Oser et al. (2010), who used cosmological parameters from WMAP3 (Spergel et al. 2007; \( h = 0.72, \Omega_m = 0.044, \Omega_{dm} = 0.26, \Omega_{\Lambda} = 0.74, \sigma_8 = 0.77, \) and \( n_s = 0.95 \)). The simulations have a dark matter particle resolution of \( m_{dm} = 3.4 \times 10^9 M_\odot \) and a baryonic mass resolution of \( m_{bar} = 5.8 \times 10^8 M_\odot \). The comoving gravitational softening lengths are \( \epsilon_{halo} = 1.236 \) kpc for the dark matter and \( \epsilon_{gas,star} = 0.556 \) kpc for the gas and star particles.

The simulations include the star formation and chemical enrichment model of Aumer et al. (2013), which allows chemical enrichment by Type I and II supernovae (SNe) and asymptotic giant branch (AGB) stars. The chemical yields are from, respectively, Iwamoto et al. (1999), Woosley & Weaver (1995), and Karakas (2010) for Type I and II SNe and AGB stars. The stellar kinetic feedback model is adopted from Núñez et al. (2017), in which winds from young massive stars, UV heating within the Strömgren spheres of young stars, three-phase SN remnant input from both Type I and Type II SN feedback, and outflows from dying low-mass AGB stars are included. The simulations include the metal diffusion model from Aumer et al. (2013), in which the metal-enriched gas particles mix their metals with neighboring gas via turbulent diffusion of gas-phase metals.

In the simulations, new collisionless black hole particles with a mass of \( 10^5 h^{-1} M_\odot \) are seeded at the center of new emerging dark matter halos with mass above \( 1 \times 10^{11} h^{-1} M_\odot \). Then they can grow via mergers with other black holes and direct accretion of gas. The gas accretion onto a black hole is estimated with a Bondi–Hoyle–Lyttleton parameterization (Hoyle & Lyttleton 1939; Bondi & Hoyle 1944; Bondi 1952). The black hole mass accretion model also includes the soft Bondi criterion that statistically limits the accretion to the gas within the Bondi radius as in Choi et al. (2012). Super-Eddington accretion is allowed in the simulations, as the accretion rate is not artificially capped at the Eddington rate. Instead, the Eddington force pushes electrons in gas particles radially away from the black hole, and the feedback processes summarized below quickly reduce the mass accretion.

The simulations incorporate mechanical active galactic nucleus (AGN) feedback, which imparts mass and momentum
**Table 1** Overview of Physical Quantities of NGC 5128 and Three Simulated Galaxies

|                  | Observation NGC 5128 | Simulation m0163 | Simulation m0125 | Simulation m0204 |
|------------------|----------------------|------------------|------------------|------------------|
| $M_{\text{vir}}$ ($M_\odot$) | $10^{12.96\pm0.18}$ | $10^{12.9}$      | $10^{13.0}$      | $10^{12.8}$      |
| $M_{\text{stellar}}$ ($M_\odot$) | $10^{11.46\pm0.12}$ | $10^{11.5}$      | $10^{11.2}$      | $10^{11.6}$      |
| $r_{\text{vir}}$ (kpc) | $400 \pm 43$         | $407.6$          | $441.7$          | $368.8$          |
| $r_{\text{eff}}$ (kpc) | $5.6 \pm 0.15$       | $5.94$           | $5.20$           | $2.50$           |

Notes:

- a This is the total mass of the Cen A group, measured with dynamics of satellites (Woodley 2006). The Cen A group virial radius is estimated accordingly ($r_{\text{vir}} \equiv r_{200}$; Rejkuba et al. 2014).
- b We adopted a distance modulus ($m-M_B=27.91$ from Harris et al. (2010) and estimated the stellar mass using an integrated magnitude of $V_I=6.2$ (van den Bergh 1976) and ($M/L_V)=7$ following Harris & Harris (2002).
- c The half-light radius of NGC 5128 is $R_{\text{eff}}=305\,\alpha$.

3.75 < $r_{\text{proj}}$/kpc < 42.5 kpc centered at $r_{\text{proj}}=40$ kpc, which corresponds to the Rejkuba et al. (2005) target field. In addition, only stellar particles within the virial radius $r < r_{\text{vir}}$ of the galaxies are selected to exclude foreground and background stars. The number of star particles used to obtain MDFs is 1100, 1531, and 715 for m0163, m125, and m0204, respectively. The number of RGB stars used to construct the observed MDF is 2058 (Rejkuba et al. 2005).

Since the limiting magnitude of the observations is 1.0–1.6 mag below the tip of the RGB, metallicity distributions are only measured for the brightest RGB stars in many observational studies. These luminous red giant stars are biased against older populations, and we correct this bias by applying a weight to each stellar particle based on its metallicity and age. Using the Yonsei–Yale model isochrones (Yi et al. 2001; Demarque et al. 2004) and assuming a Kroupa initial mass function (Kroupa 2001), we calculate the weight, i.e., the fraction of observable mass above the observation limit to the total mass of a single stellar population. We adopted the limiting magnitude of $I \sim 29$ from Rejkuba et al. (2005). The model weight is calculated for metallicities from $Z=10^{-2}$ to 0.08 and population ages from $t_{\text{age}}=1$ Myr to 14 Gyr. As the limiting magnitude of $I \sim 29$ is 1.0–1.6 mag below the RGB tip, the observable mass fraction of RGB stars to the total mass of the stellar population is higher for younger populations with $t_{\text{age}} < 1$ Gyr and smaller for older stellar populations. In order to compare our results to the observed MDFs, we apply this weight to each stellar particle when we tabulate the MDF for the simulated galaxies. Note that this correction does not dramatically alter the shape of the simulated MDFs, since the outer halo region does not contain a significant population of young stars.

We take the metallicity of each star particle in the simulations to construct the MDF. Due to the limited resolution, we treat each star particle as a single stellar population. The age and metallicity of each star particle are used to calculate a weight and correct for the observational selection effect as described above. On the other hand, the metallicity value of each RGB star is obtained by interpolating between model isochrones in observations. A single age and a fixed $\alpha$-element abundance are usually adopted for model isochrones. The stellar metallicities are obtained in a fundamentally different fashion in observations and simulations. However, the discrepancy induced by different metallicity measurement methods in observations and simulations is expected to be minor in this study, as the outer halo stars are old, with stellar age $t_{\text{age}} \sim 10$ Gyr in simulations, consistent with the commonly adopted stellar age of the isochrone fitting used in observations.

2.2. Measuring MDFs

In observations, the resolved stellar photometry is obtained for only a small target field. For example, the field of view of the Advanced Camera for Surveys (ACS) target field in Rejkuba et al. (2005) is $202\,\alpha \times 202\,\alpha$, which corresponds to 3.7 kpc x 3.7 kpc at the 3.8 Mpc distance of NGC 5128 (Harris et al. 2010). Due to the resolution limit of our simulations, we did not use a small target field to select the outer halo stars as in the observations because it would contain too few star particles to obtain a meaningful measure of the MDF. Instead, we use all star particles within a projected distance of the surrounding gas. This model mimics the observed strong wind outflows (e.g., Arav et al. 2020) launched by radiation from radiatively efficient accretion onto a black hole (e.g., Proga et al. 2000; Proga & Kallman 2004). The simulations also include Compton and photoionization heating and the associated radiation pressure effect of moderately hard X-ray radiation (∼50 keV) from the accreting black hole following Sazonov et al. (2004, 2005). This mechanical and radiative AGN feedback model is shown to effectively suppress star formation in cosmological simulations of massive galaxies (Choi et al. 2015, 2017).

In the simulations, the masses in 11 different species, H, He, C, N, O, Ne, Mg, Si, S, Ca, and Fe, are calculated explicitly for star and gas particles. The total metal abundance $Z$ is calculated using nine heavy elements and shown in units of solar metallicity $Z_\odot=0.0134$ adopted from Asplund et al. (2009).

The simulations reproduce the basic physical properties of observed massive elliptical galaxies. The most relevant observed global relation for this study is the stellar mass–metallicity relation (MMR), and the predicted stellar MMR of this simulation suite reproduces the overall shape and slope of the observed MMR (see Figure 8 in Choi et al. 2017). Choi et al. (2020) also showed that the simulations reproduce observed scaling relations between the iron abundance of the hot gas halo and X-ray luminosity.

Of 30 galaxies in the Choi et al. (2017) simulation suite, we focus on three halos, m0163, m0125, and m0204, which have comparable masses and sizes to the local elliptical galaxy NGC 5128 that we focus on in this study. The physical quantities of these example galaxies are summarized in Table 1.

3. Results

We first focus on the metallicity distribution of stars in the outer halo of galaxies within a projected radius of 37.5 kpc < $r_{\text{proj}}$ < 42.5 kpc. The projected radius of this annular region corresponds to the galactocentric distance of 0.008. The resampling of stars within a larger region (e.g., $35 < r_{\text{proj}}$/kpc < 45) also does not change the results.

9 The direction of the projection has a negligible effect on the MDF. We measured the MDF of the projected field along 100 randomly chosen directions relative to the main stellar body to test this. Changing the projection direction does not change the resulting MDF or the median metallicity. The standard deviation of the median metallicity of stars sampled along 100 projections is 0.008. The resampling of stars within a larger region (e.g., $35 < r_{\text{proj}}$/kpc < 45) also does not change the results.
the Rejkuba et al. (2005) observations of stars in NGC 5128 ($r_{\text{proj}} \sim 40$ kpc).

In Figure 1, we show MDFs of stars at $r_{\text{proj}} \sim 40$ kpc for three example simulated galaxies. The observed MDF of an outer halo field in NGC 5128 derived from the upper RGB photometry from Rejkuba et al. (2005) is also shown for comparison. The simulations can approximately reproduce the observed MDF, including its range of metallicity and the location of the peak. Both observed and simulated MDFs show a slow increase toward higher metallicities and a steeper decline after the peak. The MDFs of all simulated galaxies exhibit a peak at around $[\text{M}/\text{H}] = -0.3$, similar to the observed peak. Compared to less massive local galaxies, the metallicity distribution of this giant E/S0 galaxy is broad and moderately metal-rich, with median metallicity $[\text{M}/\text{H}] = -0.377$ (Rejkuba et al. 2005). The median value of the metallicity distributions of the simulated galaxies is $-0.367$, $-0.370$, and $-0.478$ for m0163, m0125, and m0204, respectively. The example galaxy m0204, with an effective radius $r_{\text{eff}}$ a factor of 2 smaller than NGC 5128, is the most metal-poor and shows a more extended metal-poor tail.

Individual differences in the MDFs of massive galaxies reflect a wide range of complex star formation and merger histories. To investigate the origin of stars that constitute the outer fields of massive galaxies, we traced the origin of each star particle included in the MDF of Figure 1 and checked its formation location. For halo stars within a projected radius of $37.5$ kpc $< r_{\text{proj}} < 42.5$ kpc, we find that some are made in situ, within 10% of the virial radius ($r_{10} \equiv 0.1 \times r_{\text{vir}}$) of the main halo, while most are formed ex situ, outside of $r_{10}$, and later accreted. In Figure 2, we compare the MDFs of accreted and in situ stars for each example galaxy. We find that the outer halo fields of all example galaxies mainly consist of accreted stars. The shape and peak of the MDFs of accreted stars are almost identical to those of all stars. On the other hand, in situ formed stars are mostly metal-rich with a median metallicity $[\text{M}/\text{H}] \sim -0.2$, and their MDFs lack the low-metallicity tails. The median metallicity of in situ stars is about 0.3 dex higher than that of accreted stars.
The top panels of Figure 3 show the histograms of stellar ages for the simulated galaxies. The distributions of stellar ages of in situ and accreted stars are also shown for comparison. Again, the stellar age distribution of outer halo field stars is dominated by the accreted stellar population. They are mostly old and exhibit a peak at \( \sim 11.5 \) Gyr, but there are a considerable number of young and intermediate-age stars. These young and intermediate-age stellar populations in the outer halo mainly have an accreted origin, while in situ formed stars are mostly old, except for the case of the example galaxy m0204. Compared to the other two example galaxies, the stellar population of the galaxy m0204 is older, with a dearth of stars younger than \( \sim 7 \) Gyr. Its in situ formed stellar population is younger compared to the other galaxies, with a median age of \( t_{\text{age}} \sim 9.5 \) Gyr.

To investigate the formation history of stars in the outer halo fields of simulated galaxies in detail, we show the age–metallicity relations (AMRs) of these stars in the bottom panels of Figure 3. The color of each simulated star particle scales with its formation location in units of the virial radius of the main galaxy at that time. A striking feature of Figure 3 is that the AMRs of the three example galaxies are quite different, especially for younger stars, even though their MDFs are similar (see Figure 1). This demonstrates that different elliptical galaxies march at different paces but reach very similar destinations.

The AMRs of the three example galaxies show similar trends for old stars. For all galaxies, the most metal-poor stars are the oldest. However, the oldest stars are not always the most metal-poor ones, as these galaxies have old stars that span a broad range in metallicity of \(-2.0 < [\text{M}/\text{H}] < 0.3\). This indicates that the initial chemical enrichment was fast, already reaching solar or twice-solar metallicity for the \( \sim 11–12 \) Gyr old population. This fast chemical enrichment happens within the main progenitor (in situ; dark blue symbols), as well as within the smaller galaxies where the accreted stars are made (ex situ; red symbols). These smaller systems are made at early times and contain primarily old stars, but we see that some of these systems also undergo a fast chemical enrichment at early times, adding metal-rich stellar populations to the final galaxy when they merge in.

On the other hand, the AMRs of the three example galaxies show different features for the younger stellar population. First of all, m0163 shows an extended and correlated AMR for \( t_{\text{age}} < 8 \) Gyr. This thin relation of young stars that predominantly formed around \( r \sim r_{\text{vir}} \) is similar to those predicted by noncosmological homogeneous galactic chemical evolution models (e.g., see Figure 18 of Carrera et al. 2008, and references therein). A period of slow metallicity evolution with small scatter until around 4 Gyr ago for accreted stars indicates that a small merging galaxy system underwent a period of star formation and chemical evolution. Second, m0125 also shows a thin relation of young-to-intermediate-age accreted stars, as
predicted by classical galactic chemical evolution models, but overall, this feature is less apparent, with a lack of young stars with $r_{\text{age}} < 6 \text{ Gyr}$. Lastly, m0204 has a lack of young-to-intermediate-age stars younger than 8 Gyr. It does not show a distinct correlated AMR of young stars compared to the other galaxies.

Now we investigate the formation history of stars found in the outer halo. We follow back in time every star particle that ends up within a projected radius of $37.5 \text{ kpc} < r_{\text{proj}} < 42.5 \text{ kpc}$ and $r < r_{\text{vir}}$. We check both the formation time when a star particle is born and the formation location where it is born, i.e., its distance from the galaxy center. Figure 4 visualizes the stellar origin of our fiducial field at $R \sim 40 \text{ kpc}$ for three example galaxies. The color of each simulated star particle scales with its metallicity. The histograms for the formation radii for outer halo field stars show that massive simulated galaxies’ outer halos consist mainly of accreted stars.

If we take a conventional spatial division of 10% of the virial radius $r_{\text{10}}$ for in situ versus accreted (Oser et al. 2010), the fraction of mass in accreted stars is 87.35%, 82.25%, and 86.8%, respectively, for the three galaxies. Most of these accreted stars are formed at relatively early times ($z > 3$) in small systems outside the virial radius of the galaxy but added to the parent galaxy late in its evolution. As they originate from lower-mass, lower-metallicity systems, the bulk of them are metal-poor. However, some of the accreted stars are younger and more metal-rich. The accreted stars formed as a consequence of the interactions with the main galaxy are clearly visible along the thin evolutionary tracks in Figure 4. The younger stars are more metal-rich in these evolutionary tracks, which are most visible in the case of m0163. This indicates that these small systems experience a period of star formation and chemical enrichment as they merge into the main galaxy. Depending on its recent merger history, the age distribution of stars in outer fields differs for each example galaxy. For example, m0163, which had mergers most recently, shows more prominent young stellar populations.

In order to show how the stars that populate the outer halo have migrated, we show the formation radii versus the final radii of stellar particles in the outer halo field of the three example galaxies in Figure 5. As we select the outer halo stars within a projected distance of $37.5 < r_{\text{proj}}/kpc < 42.5$ and a virial radius $r < r_{\text{vir}}$, the stars are distributed in a narrow range of final radii. However, as seen in Figure 4, their formation radii are widely distributed. This is because the bulk of the stars form ex situ, outside of the galaxy at $r/r_{\text{vir}} \sim 10^{-5}$–10, and are accreted later on. Below the dotted line, in situ formed stars are shown, i.e., the stars that have formed within the galaxy ($r/r_{\text{vir}} \sim 10^{-1}$) and then migrate outward. They are currently located in a relatively inner region compared to ex situ formed stars. The presence in the outer halo of star particles that formed in the inner region can be attributed to radial heating and major mergers (see also the discussion in Section 4.2), but they mostly occupy the inner region of the selected outer halo fields.

So far, we have focused on the metallicity distribution of stars at $r_{\text{proj}} \sim 40 \text{ kpc}$, which corresponds to the target field of the Rejkuba et al. (2005) observations. Now we study the metallicity distribution of stars in fields at larger and smaller projected radii than $r_{\text{proj}} \sim 40 \text{ kpc}$. In Figure 6, we show normalized MDFs of stars in four projected fields with average galactocentric radii of 20, 40, 60, and 90 kpc. Note that the MDFs include a smoothing of $\Delta[M/H] = 0.1$ to represent estimated observational uncertainties, and the unsmoothed MDFs are shown in Figure 7. The median metallicity of stars decreases with increasing projected distance from the center of the galaxy. The peak or mode of the MDF also decreases with increasing projected distance from the center of the galaxy. The peak or mode of the MDF also decreases with increasing projected distance from the center of the galaxy. The peak or mode of the MDF also decreases with increasing projected distance from the center of the galaxy. The peak or mode of the MDF also decreases with increasing projected distance from the center of the galaxy.

In Figure 7, we separately show the MDFs of accreted and in situ stars in each projected field at galactocentric radii of 20, 40, 60, and 90 kpc for the three example galaxies. Compared to the main outer halo field of $37.5 \text{ kpc} < r_{\text{proj}} < 42.5 \text{ kpc}$...
second row], the inner halo fields have more in situ formed stars. In the case of m0163, the in situ stars form a secondary metal-rich peak in the total MDF. The metal-rich secondary peaks in other galaxies are due to the shape of the MDF of the accreted component. As seen in Figure 3, some of the merged galaxies undergo fast chemical enrichment at early times and add metal-rich stars to the final galaxy when they merge in. With increasing galactocentric distance, there is less contribution of in situ formed stars.

Figure 8 shows the median metallicity as a function of projected distance in units of physical scale (left) and effective radius (right) for the simulated galaxies and NGC 5128. We estimate the uncertainties of the median metallicity using bootstrap resampling (Efron 1979). The observational data are from Rejkuba et al. (2014), who obtained the metallicity distributions of RGB stars out to a projected distance of 140 kpc, which corresponds to $25r_{\text{eff}}$ for NGC 5128. They also compiled the data from the previous NGC 5128 observations of Harris et al. (1999), Harris & Harris (2000), Harris & Harris (2002), and Rejkuba et al. (2005) and showed the metallicity gradient with a more metal-rich inner region and lower-metallicity outer halo, with some field-to-field metallicity variations (e.g., $r_{\text{proj}} \sim 85$ kpc). We compare the median metallicity of stars in our simulated galaxies for four fields from 20 to 90 kpc previously shown in Figure 6 to the observed metallicity profile of Rejkuba et al. (2014) and find overall good agreement. As already shown in Figure 1, m0204 has a lower median metallicity compared to NGC 5128, especially for the inner fields, for the same physical projected distance. However, the difference becomes negligible when comparing the fields’ metallicity for the projected distance in units of effective radius.

4. Discussion

4.1. The Stellar Accretion Origin of Outer Halo Stars

By tracing the origin of each stellar particle and checking its formation location, we have shown that $\sim 85\%$ of the stars in
the outer halo fields have an accreted origin (Figures 2 and 4). That means that most of the stars in the outer halos were not born there but instead were born in the much lower mass systems that have been accreted and shredded in the stellar envelopes of the early-type galaxies, as discussed in many previous studies (e.g., Naab et al. 2007; Bezanson et al. 2009; Oser et al. 2010; Hilz et al. 2013; Hirschmann et al. 2013; van Dokkum et al. 2014, 2015; Hirschmann et al. 2015). The fraction of accreted stars is higher in the outer region than in the whole galaxy, as dry minor mergers predominantly deposit stars in the outskirts of the galaxies (see Figure 7). These accreted stars are formed at relatively early times in lower-mass, lower-metallicity systems; therefore, they are mostly old (see Figure 3) and metal-poor. In particular, the metal-poor tail of the MDF in the outer halo is primarily populated by accreted stars in all three simulated galaxies (Figure 2). This is consistent with the finding of Calura et al. (2012), who showed that the low-metallicity tail (stars with $[M/H] < -4$) of the simulated halo of a Milky Way–mass galaxy mainly consists of accreted stars. However, other studies have shown that lower-mass galaxies (such as the one studied by Calura et al. 2012) have a more significant contribution from in situ star formation.
than the more massive gE-type galaxies in our study (see, e.g., Oser et al. 2010; Rodriguez-Gomez et al. 2016).

All three galaxies have not had major mergers since $z = 2$ but had many dry minor mergers of small systems, which mostly added low-metallicity stars. We found that recent gas-rich mergers can deposit metal-rich and young stars in the outer halo region. Galaxy m0163 had two recent gas-rich minor mergers at $z = 0.2$ and 0.33 that added newly formed stars. The merger at $z = 0.33$ was more massive than another with a mass ratio of $>1:8$. Galaxy m0175 also had a recent minor merger at $z = 0.7$, adding some young stars formed during the interaction, and m0204 had no gas-rich mergers recently. Despite having different merger histories, all three galaxies show comparable MDFs. The age distribution of stars, however, is more sensitive to the recent merger histories (Figure 3), as found in D’Souza & Bell (2018, 2021). We expect that the observed age distribution of the outer fields can narrow the range of allowed interactions (see also Wang et al. 2020).

### 4.2. Contribution of In Situ Formed Stars via Radial Migration

The effect of the radial migration of stars on the stellar metallicity distribution has been studied mainly for the Galactic disk, and it has been shown that stellar radial migration broadens MDFs and produces a greater dispersion (Di Matteo et al. 2013; Grand et al. 2015; Halle et al. 2015). Here we focus on the effect of “outward” radial migration of centrally formed in situ stars.

Although the majority of stars in outer halos are accreted in our fiducial field at a projected radius $R \sim 40$ kpc, 12%–17% of stars are formed in situ within the main progenitor in the simulations (Figure 4). Some of them formed in the central region and then migrated out to larger radii (Figure 5). The majority of the centrally formed in situ stars remain in the central part of the galaxy (see Oser et al. 2010, 2012; Hirschmann et al. 2015), but some of the in situ stars formed at high redshift can migrate over quite large distances, over 10 kpc since $z = 2$ (Choi et al. 2018; see their Figure 5).

This migration of stars is a result of a combination of several physical processes. First of all, gas ejection by outflows can result in the expansion of the stars in the central region (Hills 1980). Slow gas mass loss associated with the death of old stars such as AGB winds can adiabatically expand the central region. Also, rapid gas mass loss via SN- and AGN-driven winds, which are very common in massive systems, as shown in Brennan et al. (2018), can cause an impulsive expansion (Biermann & Shapiro 1979; Fan et al. 2008).

Second, the centrally formed stars can gain angular momentum via dynamical interactions during major mergers and migrate outward. For example, Hirschmann et al. (2015) showed that galaxies that have experienced recent major mergers can have a significant fraction of centrally formed in situ stars that have migrated outward to the outskirts of galaxies.

Lastly, a binary black hole formed by a merger of two galaxies scours the stars from the nucleus as the binary hardens (Milosavljević & Merritt 2001). The ejection of surrounding stars enables the energy liberated by the shrinking of the binary to evacuate the central region and is believed to produce the observed cores in the light profiles of massive galaxies (e.g., Faber et al. 1997). The simulations presented in this paper include black hole mergers and the associated heating effect of the shrinking orbit of a binary system. However, we expect the effect of the black hole binary scouring on the ejection of in situ formed stars to be negligible in the simulations due to the insufficient resolution.

Since recently formed in situ stars would not have had enough time to migrate out to larger radii, the in situ stars found in the outskirts of galaxies are primarily old (Figure 3). Even though they are born at high redshift, around $z \sim 3$, their metallicity is much higher than that of accreted stars (see Figures 2 and 4). This is because the central regions of the most massive progenitors underwent rapid chemical enrichment. In our fiducial outer field at $r_{proj} \sim 40$ kpc of NGC 5128, the contribution of in situ stars that have migrated out to that distance is likely to be minor, but we expect that a metal-rich in situ star population can be dominant in the inner region of galaxy halos (Figure 7; and see more discussion in Section 4.3).
4.3. Variations in the MDF with Radial Distance

The study of metallicity gradients in elliptical galaxies has had a long history since de Vaucouleurs (1961). Due to a decline in metallicity with increasing radius, elliptical galaxies are generally observed to be bluer at larger radii by photometric studies (Strom & Strom 1978; Zibetti et al. 2005; Suh et al. 2010; Tortora et al. 2010; Zibetti et al. 2020). This is confirmed by spectroscopic studies that have looked at the gradients in the equivalent width of metal lines (Fisher et al. 1995; Baes et al. 2007). The metallicity gradients of elliptical galaxies have typically been studied within $r_{\text{eff}}$ but recently observed out to larger radii of $\sim 8r_{\text{eff}}$ (e.g., Coccato et al. 2010; Greene et al. 2012, 2013; La Barbera et al. 2012). Via resolved stellar photometry, Rejkuba et al. (2014) studied the metallicity gradient even further out, to $25r_{\text{eff}}$. They obtained the MDFs of individual RGB stars in each ACS field and investigated the halo metallicity gradient by measuring the median metallicity of stars as functions of the projected distance from the center of NGC 5128. We compare the observed median metallicity of stars from Rejkuba et al. (2014) to the simulations and find a consistent decline in metallicity with the projected distance (Figure 8). We find a change in the median $[M/H]$, $\Delta[M/H] \sim -0.3$, 0.2, and 0.23 dex over 40–90 kpc, for m0163, m0125, and m0204, respectively. This corresponds to a gradient of $\sim 0.006$, 0.004, and 0.0046 dex kpc$^{-1}$, which is comparable to or modestly higher than the observed value found by Crnojević et al. (2013) via a VLT/VIMOS survey.

Not only the median metallicity but also the overall shape of MDFs differs with the projected distance. The MDF of the outermost halo field shows an extended metal-poor tail for all simulated galaxies (Figure 7). This is consistent with the finding of Harris & Harris (2002), who showed a longer and thicker tail toward lower metallicity in the MDF of the outer halo field compared to that of the inner halo field (see their Figure 9). Crnojević et al. (2013) derived MDFs of NGC 5128 up to $\sim 85$ kpc and also found a thicker metal-poor tail in the outer region. Lee & Jang (2016) also showed that the outer halo field of a standard elliptical galaxy, M105, exhibits an extended metal-poor tail compared to the inner region (see their Figure 12).

In contrast, the inner halos of elliptical galaxies are observed to have a prominent metal-rich population and sometimes two distinct subpopulations (Harris & Harris 2002; Lee & Jang 2016). Inner halos tend to have more contribution from centrally formed in situ stars via radial migration, sometimes showing a distinct metal-rich subpopulation in MDFs (Figures 6 and 7). The population mixture of in situ and accreted stars can dominate the transition of the MDF for the inner halo regions. This is consistent with the sharply declining radial number density profile of the metal-rich RGB stars in the outer region of M105 found in Lee & Jang (2016). Bird et al. (2015) found no evidence of a steep density falloff of metal-rich stars ($[M/H] \geq -0.7$) within 65 kpc in NGC 5128, but the transition must lie further out, as in our simulated galaxies.

4.4. Age Distribution of Outer Halo Stars

Even though we applied a weighting function when we calculated the MDFs (see Section 2.2), the stellar metallicities obtained in observations and from simulations are derived in a fundamentally different fashion. In observations, photometric metallicities are derived by assuming a single age and a fixed $\alpha$-element abundance. Then, individual metallicity values of stars are obtained by interpolating between model isochrones with different metallicities. For the simulations, we take the age of each star particle as shown in Figure 3. However, the discrepancy between the observed and simulated age is expected to be minor, as the bulk of outer halo stars are born early with $t_{\text{age}} \sim 10$ Gyr in simulations, consistent with the commonly adopted stellar age of the isochrone fitting.

We found that most stars are old in the outer halo field of simulated galaxies (Figure 3). Rejkuba et al. (2011) also found that the bulk of outer halo stars are old in the outer field of NGC 5128. They constructed synthetic color–magnitude diagrams (CMDs) with varying star formation histories to fit a matched CMD to the data and found that two burst models best fit the data. They found that 70%–80% of the stars are old, with $t_{\text{age}} \sim 12$ Gyr, and old stellar populations with the full metallicity range of the models ($Z = 0.0001–0.04$) are needed to reproduce the observed RGB stars in their synthetic CMD models. This is consistent with our findings that all simulated galaxies have old stars that span a broad range in metallicity of $-2.0 < [M/H] < 0.3$ (Figure 3).

There are some contributions from young and intermediate-age stars in simulated galaxies. Rejkuba et al. (2011) found that 20%–30% of stars are young, with $t_{\text{age}} \sim 2–4$ Gyr in the outer field of NGC 5128. Rejkuba et al. (2022) recently confirmed this result, finding that a young stellar population with $t_{\text{age}} \sim 4$ Gyr or younger is needed to reproduce the observed excess of stars above the tip of the RGB. Among our three simulated galaxies, only m0163 shows a considerable number of young stars with $t_{\text{age}} \sim 4$ Gyr comparable to these recent findings.

4.5. Caveats and Limitations

We found excellent agreement between the simulation predictions for MDFs and the observations of NGC 5128, but there remains uncertainty in the models. Adjusting the parameterization of the subgrid routines of stellar and AGN feedback can alter the MDF outputs. The AGN feedback is found to play the most dominant role in reproducing the fundamental physical properties of observed massive elliptical galaxies in the simulations (Choi et al. 2017). However, the stellar feedback is expected to play an essential role in reproducing MDFs, as stellar metallicities of low-mass satellite galaxies that make up the ex situ stellar halo could be very sensitive to stellar feedback. Moreover, the physical mechanisms that are not included in the simulations, such as the effects of relativistic AGN jets or cosmic rays, can also affect the results. The significance of each effect on the resulting MDFs will be explored in detail in future work.

Although our simulations represent a good match to the observed MDF of NGC 5128, the current results may not be representative of massive elliptical galaxies in general. We present a minimal number of simulated samples applicable to a single observed galaxy. In order to draw general conclusions on massive elliptical galaxies and their MDFs, it is necessary to study a more significant number of simulated elliptical galaxy samples from a cosmological volume simulation such as Illustris-TNG (Nelson et al. 2018), EAGLE (Schaye et al. 2015), or SIMBA (Davé et al. 2019). Analyzing the simulated MDFs of elliptical galaxies with different star formation and stellar assembly histories and group environments will help us...
better understand the complex formation history of elliptical galaxies. We reserve this for future work.

As discussed in Section 2.2, we did not use a small target field to select the outer halo stars as in observations due to the limited resolution. Instead, we used all stellar particles within a projected annulus to sample enough star particles to obtain MDFs. Although substructure is expected to be present in the outer halo, and Rejkuba et al. (2014) also showed the large field-by-field variation in the outer field of galaxies, field-to-field scatter cannot be studied with current simulations due to small number statistics. To check the variations between different fields in the outer halo, much higher resolution simulations will be needed, which is beyond the scope of this paper. This subject is reserved for future work.

4.6. Future Perspective

A detailed study of the stellar populations in nearby elliptical galaxies will allow us to better understand the physical processes involved in the formation and growth of massive elliptical galaxies. The analysis of the CMD of the resolved stars is the most direct way to estimate the metallicity and age of stellar populations. However, the amount of data is still limited, as it has to come from HST or a ground-based telescope under very good seeing conditions (Cromjević et al. 2013). Therefore, most of the stellar mass of NGC 5128 is still left unexplored. With the James Webb Space Telescope (JWST) and the next generation of large-aperture ground-based telescopes, it will be possible to map the metallicity distribution over the whole galaxy, even for the crowded inner regions (Schreiber et al. 2014).

The JWST’s ability to resolve individual stars will offer the opportunity to perform accurate stellar photometry in crowded fields of local galaxies that are within reach of the HST. Moreover, with its much higher spatial resolution and higher sensitivity, JWST will bring more distant targets within reach, allowing us to study in detail the stellar populations in distant ellipticals to the Leo group objects at $D \sim 10$ Mpc and then outward to Virgo ($D \sim 16$ Mpc) and Fornax ($D \sim 19$ Mpc). By resolving individual RGB stars and studying their calibrated infrared features, one can determine their metallicity distribution (e.g., Valenti et al. 2006). As the ellipticals may result from a wide range of formation histories, a detailed comparison of metallicity distributions for a more significant number of observed elliptical samples to models will allow us to better understand how ellipticals formed and have evolved.

5. Summary

We investigate the MDFs of stars in the halos of simulated elliptical galaxies and compare them to the resolved stellar photometry observations of the local lE galaxy NGC 5128. Our main findings are summarized as follows.

1. The predicted MDFs from simulations are in good qualitative agreement with the observed MDF of NGC 5128. The correspondence between simulated and observed MDFs indicates that the treatment of metal production, expulsion, and accretion of simulations is approximately correct.

2. Using cosmological simulations of massive galaxy formation, we predict that most of the stars in the outer fields of massive galaxies have an “accreted” origin, formed in other small galaxies and later merged in.

3. The contribution of centrally formed in situ stars is subdominant in the outer halo but can be dominant in the inner regions, as they can more effectively migrate outward from the center.

4. We find a decline in median metallicity with the projected galactocentric distance, consistent with the observed median metallicity of stars from Rejkuba et al. (2014). We also find that the overall shape of the MDFs differs with the projected distance; i.e., the MDF of the outer halo field shows a more extended metal-poor tail.

5. This study presents a limited number of simulated galaxy samples compared to a single observed galaxy, NGC 5128. However, the results presented here can provide the baseline for future studies on comparing MDFs in simulations and observations of elliptical galaxies. Resolved stellar photometry from upcoming telescope facilities such as JWST will provide more constraints for galaxy formation models. Combining these data with more galaxy samples from larger-volume simulations will enable us to refine our models of massive galaxy formation.

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ORCID iDs

Ena Choi @ https://orcid.org/0000-0002-8131-6378
Jeremiah P. Ostriker @ https://orcid.org/0000-0002-6405-9904
Michaela Hirschmann @ https://orcid.org/0000-0002-3301-3321
Thorsten Naab @ https://orcid.org/0000-0002-7314-2558

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