A critical analysis of the UV-continuum slopes ($\beta$) of high-redshift galaxies; no evidence (yet) for extreme stellar populations at $z > 6$.

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13 January 2013

ABSTRACT
Following the discovery of the first significant samples of galaxies at $z > 6.5$ with Wide Field Camera 3/Infrared (WFC3/IR) on board Hubble Space Telescope (HST), it has been claimed that the faintest high-redshift galaxies display extremely blue ultraviolet (UV) continuum slopes, with a UV power-law index $\beta \simeq -3$ (where $f_\lambda \propto \lambda^\beta$). Such slopes are bluer than previously reported for any other galaxy population, and are most readily explained theoretically by extinction-free, young, very low-metallicity stellar populations with a high ionizing photon escape fraction. Here we undertake a critical study of the evidence for such extreme values of $\beta$, combining three new WFC3/IR-selected samples of galaxies spanning nearly two decades in UV luminosity over the redshift range $z \simeq 4.5 - 8$. We explore the impact of inclusion/exclusion of less robust high-redshift candidates, and use the varying depths of the samples to explore the effects of noise and selection bias at a given ultraviolet luminosity. Simple data-consistency arguments suggest that artificially blue average values of $\beta$ can result when the analysis is extended into the deepest $\simeq 0.5$ mag bin of these WFC3/IR-selected galaxy samples, regardless of the actual luminosity or redshift range probed. By confining attention to robust high-redshift galaxy candidates, with at least one 8-\sigma detection in the WFC3/IR imaging, we find that the average value of $\beta$ is consistent with $\langle \beta \rangle = -2.05 \pm 0.10$ over the redshift range $z = 5 - 7$, and the UV absolute magnitude range $-22 < M_{UV,AB} < -18$, and that $\langle \beta \rangle$ shows no significant trend with either redshift or $M_{UV}$. We create and analyse a set of simple end-to-end simulations based on the WFC3/IR+ACS Hubble Ultra Deep Field (HUDF) and Early Release Science datasets which demonstrate that a bias towards artificially low/blue average values of $\beta$ is indeed “expected” when the UV slope analysis is extended towards the source detection threshold, and conclude that there is as yet no clear evidence for UV slopes significantly bluer than $\beta \simeq -2$, the typical value displayed by the bluest star-forming galaxies at more modest redshifts. A robust measurement of $\langle \beta \rangle$ for the faintest galaxies at $z \simeq 7$ (and indeed $z \simeq 8$) remains a key observational goal, as it provides a fundamental test for high escape fractions from a potentially abundant source of reionizing photons. This goal is achievable with HST, but requires still deeper WFC3/IR imaging in the HUDF.

Key words: galaxies: high-redshift - galaxies: evolution - galaxies: formation - galaxies: starburst - cosmology: reionization

1 INTRODUCTION

The first galaxies, by definition, are expected to contain very young stellar populations of very low metallicity. However, the possibility
of the sensitivity required to detect this line at $z > 7$ will certainly not be available until the *James Webb Space Telescope* (JWST), and even then some theoretical predictions indicate that it is unlikely to be found in detectable objects (Salvaterra, Ferrara &Dayal 2011, but see also Pawlik, Milosavljevic & Bromm 2011).

By necessity, therefore, recent attention has focussed on whether the broad-band near-infrared photometry which has now been successfully used to discover galaxies at $z \simeq 6 - 8.5$ (e.g. McLure et al. 2010; Oesch et al. 2010; Bouwens et al. 2010a; Bunker et al. 2010; Finkelstein et al. 2010; Vanzella et al. 2011) can actually be used to establish the rest-frame continuum slopes of the highest redshift galaxies. Specifically, very young, metal-poor stellar populations are arguably expected to result in substantially bluer continuum slopes around $\lambda_{rest} \simeq 1500\AA$ than have been detected to date in galaxies discovered at any lower redshift $z < 6.5$ (e.g. Steidel et al. 1999; Meurer et al. 1999; Adelberger & Steidel 2000; Ouchi et al. 2004; Stanway et al. 2005; Bouwens et al. 2006; Hathi et al. 2008; Bouwens et al. 2009; Erb et al. 2010).

It has become the normal convention to parameterise the ultraviolet continuum slopes of galaxies in terms of a power-law index, $\beta$, where $f_{\lambda} \propto \lambda^{\beta}$ (e.g. Meurer et al. 1999); thus, $\beta = -2$ corresponds to a source which has a flat spectrum in terms of $f_{\nu}$, and hence has zero colour in the AB magnitude system. As discussed by several authors, while the bluest galaxies observed at $z \simeq 3 - 4$ have $\beta \simeq -2$, values as low (i.e. blue) as $\beta \simeq -3$ can in principle be produced by a young, low-metallicity stellar population (e.g. Bouwens et al. 2010b; Schaerer 2002). However, for this idealized prediction to actually be realized in practice, several conditions have to be satisfied simultaneously, namely i) the stellar population has to be very young (e.g. $t < 30\,\text{Myr}$ for $Z \simeq 10^{-2}\,Z_{\odot}$, or $t < 3\,\text{Myr}$ for $Z \simeq 10^{-2}\,Z_{\odot}$), ii) the starlight must obviously be completely free from any significant dust extinction, and iii) the starlight must also not be significantly contaminated by (redder) nebular continuum (a condition which has important implications for UV photon escape fraction, and hence reionization – see, for example, Robertson et al. 2010).

For this reason, the recent report by Bouwens et al. (2010b) (supported to some extent by Finkelstein et al. 2010) that the faintest galaxies detected at $z > 6.5$ do indeed display an average value of $\langle \beta \rangle = -3.0 \pm 0.2$ is both exciting and arguably surprising enough to merit further detailed and independent investigation. This is especially the case because some authors are already beginning to assume that the existence of such extreme blue slopes is a robust result, already ripe for detailed theoretical interpretation (e.g. Taniguchi et al. 2010).

The aim of this paper is to carefully assess whether the current *HST* WFC3 data do indeed provide clear evidence for such extremely blue slopes in faint galaxies at $z \simeq 7$. There are a number of potentially subtle biases which can affect the determination of UV continuum slopes from the WFC3/IR data, especially when, as is inevitably the case for the faintest objects, the results have to be based on the average colours of galaxies whose individual $\beta$ values have associated errors which can be as large as $\Delta \beta \simeq \pm1.5$. To check for, and attempt to quantify, the extent of any such biases we undertake two different approaches in this paper. First, we take advantage of the dynamic range offered by the available public WFC3/IR imaging to explore how derived values of $\beta$ (and average values $\langle \beta \rangle$) depend on galaxy candidate robustness and signal-noise ratio as we approach the flux limit of a given survey. Second, we undertake and analyse a set of fairly simple (but complete end-to-end) simulations to explore what apparent values of (and trends in) $\langle \beta \rangle$ would be deduced from the existing WFC3/IR data for different assumed input values of $\beta = -2, -2.5, -3$ combined with realistic estimates of the faint-end slope of the $z \simeq 7$ galaxy luminosity function.

The layout of this paper is as follows. First, in Section 2 we briefly review how we have selected three new, high-redshift galaxy samples from the WFC3/IR+ACS+IRAC imaging of the Hubble Ultra Deep Field (HUDF), the HUDF Parallel Field 2 (HUDF09-2), and the Early Release Science imaging (ERS) of the northern portion of GOODS-South. The reduction of the *HST* data, the deconvolution of the *Spitzer* IRAC data, and the extraction, analysis, classification and redshift estimation of the galaxies uncovered from this imaging are described in detail in McLure et al. (2011), as this underpins the extraction of a new robust galaxy sample at $6 < z < 8.7$ which is the focus of the McLure et al. (2011) study. In this study we retain not only the robust $z > 6$ sources detailed in McLure et al. (2011), but all galaxies from the larger parent sample with acceptable redshift solutions at $z > 4.5$, which are classified as either ROBUST or UNCLEAR. This allows us to explore trends in $\beta$ over a reasonably wide range in redshift ($5 < z < 8$) and UV luminosity ($-22 < M_{UV, AB} < -18$), and also to explore potential biases introduced by the exclusion or inclusion of galaxies with less robust photometric redshifts. In Section 3 we explain how we determined the rest-frame UV continuum slope, $\beta$, for the galaxies extracted from the different imaging datasets at different redshifts. Then, in Section 4 we present and analyse our results, and demonstrate what level of data quality is actually required to achieve internally consistent results between the different galaxy samples uncovered from surveys of varying depths. We move on to describe and analyse our simulations in Section 5 before discussing the implications of our findings in Section 6. A summary of our conclusions is then presented in Section 7. All magnitudes are quoted in the AB system (Oke & Gunn 1983) and any cosmological calculations assume $\Omega_M = 0.3$, $\Omega_{\Lambda} = 0.7$, and $H_0 = 70\,\text{km}\,\text{s}^{-1}\,\text{Mpc}^{-1}$.

## 2 GALAXY SAMPLES

### 2.1 Basic sample production

The candidate galaxies were all selected from our own reductions of the publicly available near-infrared WFC3/IR imaging of the HUDF, ERS and HUDF09-2 fields, as described in McLure et al. (2011) (we note that the HUDF WFC3/IR imaging is the same year 1, 2009, imaging as utilised in McLure et al. 2010). In brief, candidate selection in all three fields was undertaken by first selecting sources with SEXTRACTOR (Bertin & Arnouts 1996) down to a deep signal:noise limit in each of the WFC3/IR $Y_{105}/Y_{098}$, $J_{125}$ and $H_{160}$ images, and then forming the superset of near-infrared selected sources by merging these catalogues.

Then, as again detailed in McLure et al. (2011), photometric redshifts (with associated probability distributions) were derived for all potential sources based on 0.6-arcsec diameter flux-density measurements made on the available *HST* ACS optical imaging, the WFC3/IR imaging, and the *Spitzer* IRAC imaging (after deconvolution of the IRAC images based on the WFC3/IR $H_{160}$ or $J_{125}$ data).

The samples were then culled to retain only sources with an acceptable solution at redshift $z > 4.5$ (i.e. redshift solutions with a formally acceptable value of $\chi^2$, typically $\chi^2 < 10$ given the number of data points and model free parameters). All candidate objects were then visually inspected, and rejected from the catalogue if they lay too near to the perimeter of the imaging, or too
Figure 1. Plots of $\beta$ versus redshift, $z$, for all sources in the HUDF sample (left), the HUDF09-2 sample (centre), and the ERS sample (right). Filled symbols indicate ROBUST sources, open symbols indicate UNCLEAR sources which have acceptable alternative low-redshift solutions.

Figure 2. Plots of $\beta$ versus UV absolute magnitude, $M_{1500}$, for all sources in the HUDF sample (left), the HUDF09-2 sample (centre), and the ERS sample (right). Filled symbols indicate ROBUST sources, open symbols indicate UNCLEAR sources which have acceptable alternative low-redshift solutions.

close to bright sources (a cull that is reflected in the effective survey areas quoted by McLure et al. 2011). Any remaining suspected pseudo sources arising from image artefacts were also removed at this stage.

Finally, all of the ACS+WFC3/IR+IRAC spectral energy distribution (SED) fits were inspected, and the sources classified as either ROBUST or UNCLEAR depending on whether the alternative low-redshift solution could be excluded at $>2$-$\sigma$ on the basis of $\Delta\chi^2 > 4$. We note here that the ratio of ROBUST:UNCLEAR sources varies substantially between the fields, being $\approx 2:1$ in the HUDF, $\approx 1:1$ in the ERS, and $\approx 1:2$ in HUDF09-2. This is primarily due to the variation in the depths of the available optical ACS imaging, relative to the new WFC3/IR near-infrared imaging, as discussed further below.

Absolute rest-frame UV magnitudes, $M_{1500}$, have been calculated for all objects by integrating the spectral energy distribution of the best-fitting evolutionary synthesis model (see McLure et al. 2011) through a synthetic “narrow-band” filter of rest-frame width 100 Å and correcting to total magnitude (from the 0.6-arcsec aperture magnitudes on which the SED fitting was based) via subtraction of a global aperture correction of 0.25 mag.

2.2 HUDF

In the HUDF the high-redshift galaxy sample reported by McLure et al. (2010) has now been superceded by the galaxy sample extracted by McLure et al. (2011). The new parent sample utilised here includes Spitzer IRAC detections/limits in the selection process, and extends to lower redshift to include all objects with an acceptable primary redshift solution at $z > 4.5$.

The resulting HUDF sample contains a total of 147 candidate galaxies with $z_{\text{phot}} > 4.5$. Within this master sample, 95 sources are considered ROBUST according to the criterion that the alternative lower-redshift solution can be rejected with better than $2$-$\sigma$ confidence (i.e. $\Delta\chi^2 > 4$). The relatively high fraction of robust high-redshift sources in this field reflects in large part the extreme depth of the associated optical ACS imaging in the HUDF, which helps to establish the robustness of any potential Lyman breaks.

As shown in Figs 1 and 2, the final HUDF galaxy sample at $z > 4.5$ extends to $z > 8$, and samples a rest-frame UV luminosity range corresponding to $-21 < M_{1500} < -17$ (AB). However, with one exception, ROBUST sources are confined to $-21 < M_{1500} < -18$ (AB).
2.3 HUDF09-2

The WFC3/IR imaging of the HUDF09-2 (HUDF Parallel 2) field utilised here is only 0.07 mag shallower than the 2009 HUDF WFC3/IR imaging in the $J_{125}$ band, and covers a similar area. The extracted parent sample is thus comparable in size, but due to the shallower depth of available optical ACS imaging, the fraction of ROBUST:UNCLEAR sources is much lower (see McLure et al. 2011).

The HUDF09-2 sample used here contains 135 candidate galaxies with $z_{\text{phot}} > 4.5$. Within this master sample, 49 sources are considered ROBUST according to the criterion that the alternative lower-redshift solution can be rejected with better than 2-$\sigma$ confidence (i.e. $\Delta \chi^{2} > 4$).

As shown in Figs 1 and 2, the final HUDF09-2 galaxy sample at $z > 4.5$ again extends to $z > 8$, and samples a rest-frame UV luminosity range corresponding to $-21 < M_{1500} < -17$ (AB). However, in this case, ROBUST sources are basically confined to $-21 < M_{1500} < -18.5$ (AB).

2.4 ERS

The ERS WFC3/IR imaging of the northern portion of GOODS-South covers an area $\simeq$ 10 times larger than each of the above-mentioned ultra-deep fields, but is typically a magnitude shallower. In addition, the $Y_{098}$ filter was utilised in the ERS observations, rather than $Y_{105}$, making the $Y$-band imaging even shallower. Because our galaxy selection does not involve specific colour cuts, this does not complicate our redshift completeness (c.f. Oesch et al. 2010, Bouwens et al. 2010a) but this, in combination with optical data limited to GOODS depth, does mean that about half of the ERS sample is classified as UNCLEAR.

The ERS sample used here contains 337 candidate galaxies with $z_{\text{phot}} > 4.5$. Within this master sample, 160 sources are considered ROBUST according to the criterion that the alternative lower-redshift solution can be rejected with better than 2-$\sigma$ confidence (i.e. $\Delta \chi^{2} > 4$).

As shown in Figs 1 and 2, the final ERS galaxy sample at $z > 4.5$ extends to $z > 8$, and samples a brighter rest-frame UV luminosity range corresponding to $-22 < M_{1500} < -19$ (AB).

3 MEASUREMENT OF UV CONTINUUM SLOPES

As already mentioned, the standard convention is to characterise the rest-frame UV continuum slope via a power-law index, $\beta$, where $f_\lambda \propto \lambda^\beta$.

Given the effective wavelengths of the WFC3/IR filters of interest here ($Y_{098}$: $\lambda_{\text{eff}}$=9864Å; $Y_{105}$: $\lambda_{\text{eff}}$=10552Å; $J_{125}$: $\lambda_{\text{eff}}$=12486Å; $H_{160}$: $\lambda_{\text{eff}}$=15369Å) the relevant conversions from AB mag colours to $\beta$ are:

$$\beta = 4.43(J_{125} - H_{160}) - 2$$ (1)

$$\beta = 5.47(Y_{105} - J_{125}) - 2$$ (2)

$$\beta = 3.91(Y_{098} - J_{125}) - 2$$ (3)

Choosing between the latter two options is dictated by which $Y$-band filter was used in the observations, but otherwise the choice is determined by the estimated redshift of the source. Specifically, at $z_{\text{est}} > 6.5$, both the Lyman-break and any potential Lyman-$\alpha$ emission can enter the $Y$-band (which cuts in at 9000Å), thus contaminating any measure of $\beta$. Given the uncertainties in $z_{\text{est}}$ we therefore use equation (1) for any source with $z_{\text{est}} > 6.5$, and equations (2) or (3) as appropriate at lower redshift (to ensure we sample comparable rest-frame wavelengths at all redshifts).

We also note that, at $z_{\text{est}} > 8$, both the Lyman-break and any potential Lyman-$\alpha$ emission can enter the $J_{125}$-band (which cuts in at 11000Å), and hence, at least for the current photometric dataset, any values of $\beta$ derived for sources at $z_{\text{est}} > 8$ should not be taken seriously (this is why neither Bouwens et al. (2010b) nor Finkelstein et al. (2010) attempted measurement of $\beta$ at $z \simeq 8$). However, in reality, after application of the galaxy sample quality control described below, only one galaxy candidate at $z_{\text{est}} > 8$ survives (in the HUDF09-2 field) for inclusion in the calculation.

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Figure 3. Plots of $\beta$ versus redshift $z$, and $\beta$ versus UV absolute magnitude $M_{1500}$, for all the ROBUST sources in the 3 samples (blue=HUDF, green=HUDF09-2, red=ERS).
of average values of $\beta$. Finally, we note that equation (1) above differs very slightly from the relation adopted by Bouwens et al. (2010b), which is $\beta = 4.29(J_{125} - H_{160}) - 2$, but the differences in derived values of $\beta$ are completely insignificant in the current context (e.g. for $J_{125} - H_{160} = -0.2$, the Bouwens et al. relation yields $\beta = -2.86$, while equation (1) yields $\beta = -2.89$).

4 RESULTS

4.1 Raw results

In Figs 1 and 2 we plot the raw values of $\beta$ for each source in the HUDF, HUDF09-2 and ERS samples versus redshift, $z$, and UV absolute magnitude, $M_{1500}$. In each plot the sources classified as ROBUST are indicated by the filled symbols, and those classified as UNCLEAR are indicated by the open symbols. As well as illustrating the range of redshift and UV luminosity probed by each galaxy sample, these plots dramatically illustrate what an extreme range of apparent individual values of $\beta$ results from the photometric uncertainty in colour, especially in the fainter luminosity bins probed by each sample. In general it can be seen that a large fraction of the faintest galaxies are classified as UNCLEAR. This simply reflects a lack of compelling evidence that the continuum above the putative Lyman break is blue enough to rule out a lower-redshift (possibly dusty) solution. We return to this point later in the paper, when discussing the results of the simulations in Sections 5 and 6.

The other point to note from Fig. 2 is that all three samples contain ROBUST sources with apparent values of $\beta$ as extreme as $\beta < -5$. We have not plotted error bars on individual $\beta$ values in Fig. 2, but as discussed and plotted in McLure et al. (2011), these individual values are of course highly uncertain, with $\Delta \beta \simeq \pm 1.5$ or even larger. The fact that photometric uncertainty must play a major role in producing these extreme values of $\beta$ is revealed in Fig. 2 by the fact that the plume of extremely blue/lowlow $\beta$ values emerges at a different absolute magnitude in the different samples.

To illustrate this more clearly we plot all three samples of ROBUST sources together in Fig. 3. It can be seen that very blue sources with apparent values of $\beta < -4$ emerge in the ERS sample at $M_{1500} \simeq -20$, whereas in the deeper HUDF data the emergence of such apparently extreme sources is delayed until $M_{1500} > -18.7$. The impact on the scatter in $\beta$ of approaching the flux-density limit is perhaps illustrated more clearly in Fig. 4 where we confine attention to $z > 6$, and plot $\beta$ versus observed $J_{125}$.

Of course, while photometric scatter inevitably causes the apparent range of $\beta$ to rapidly increase as the sample flux limit is approached, there are also a large number of galaxies in the final luminosity bin probed by each sample, so moderately accurate measures of the average value of $\langle \beta \rangle$ can in principle still be derived. Therefore the key issue, which we now explore, is how the average value of $\langle \beta \rangle$ is affected by the inclusion or exclusion of ROBUST/UNCLEAR sources, and also the signal/noise ratio limit of the galaxy catalogue.

4.2 Quality control

In Fig. 5 we have divided the three-field sample into 3 redshift bins, and binned the data into luminosity bins 1 magnitude wide. We therefore plot the average value of $\langle \beta \rangle$ (with errors) and in each plot show the sample-to-sample variation and the final overall average and standard error.

The top row of plots shows the results as computed from all the individual data points shown in Figs. 1 and 2, including both ROBUST and UNCLEAR sources. The second row shows the effect of including only the ROBUST sources. Finally, the third row shows the effect of further limiting the ROBUST samples to contain only objects which have at least one 8-\(\sigma\) near-infrared detection in the WFC3/IR data.

This set of plots reveals some interesting trends in the data which can be summarized as follows. First, it can be seen that restricting the sample to ROBUST sources only has the general effect of moving $\langle \beta \rangle$ to lower (i.e. bluer) values at virtually all redshifts and luminosities. Some of this effect may be due to the (desirable) removal of lower-redshift interlopers from the high-redshift galaxy samples. However, some of this shift could also be due to a bias introduced by the fact that a blue UV continuum slope increases the chance that a source will be classified as ROBUST, especially in the absence of a high signal/noise ratio break. This move to the blue is most dramatic in the faintest magnitude bin; taken at face value the middle row of plots in Fig. 5 suggests that galaxies with $M_{UV,AB} \simeq -18.5$ have a typical UV continuum slope which evolves rapidly with redshift, with $\langle \beta \rangle \simeq -2.2$ at $z \simeq 5$, $\langle \beta \rangle \simeq -2.5$ at $z \simeq 6$, and $\langle \beta \rangle \simeq -3$ at $z \simeq 7$. This is clearly fairly similar to the trend reported by Bouwens et al. (2010b).

However, it is also very clear that, especially in the faintest luminosity bins, there are huge sample-to-sample variations with, for example, the ERS sample delivering very blue values of $\langle \beta \rangle$ in the $M_{UV,AB} \simeq -19.5$ bin at $z \simeq 7$ compared to either of
the deeper HUDF and HUDF09-2 samples. This is basically the effect of the plume to low values of $\beta$ seen at the ERS flux limit as shown in Fig. 4. To reconcile the results from the different samples in the luminosity bins in which they overlap, we found it necessary to insist on a minimum signal:noise ratio requirement. To avoid introducing any further colour bias we simply chose to insist that every object retained in the final, refined sample was detected in at least one WFC3/IR near-infrared passband at a minimum level of 8-σ. The impact of this further level of quality control is then shown in the bottom row of plots in Fig. 5. No longer do the different samples deliver substantially different average values of $\langle \beta \rangle$, and it can be seen that the very low values of $\langle \beta \rangle$ were indeed largely resulting from the lowest signal:noise ratio sources. Importantly, with this level of further quality control, we are left with only one HUDF object in the $M_{UV,AB} \simeq -18.5$ bin at $z \simeq 7$, and hence cannot plot a meaningful average value of $\langle \beta \rangle$. At $z = 6$, where we can still probe this luminosity bin, the evidence for $\langle \beta \rangle$ being significantly bluer than $\langle \beta \rangle = -2$ has disappeared.

This final result is summarized in Fig. 6, where we overplot the dependence of $\langle \beta \rangle$ on $M_{UV,AB}$ as a function of redshift. The derived datapoints shown in Fig. 6 are tabulated in Table 1. Clearly, these results are consistent with $\langle \beta \rangle = -2$ over the full redshift and luminosity range which can be probed with these data. At the bright end they are also in good agreement with the results derived by both Bouwens et al. (2010b) and Finkelstein et al. (2010), so any disagreement is really confined to $M_{UV} > -20$.

Of course, it might be argued that by insisting on rejecting the lowest signal:noise ratio sources, we have effectively “thrown away” the “evidence” for how $\beta$ behaves at the faintest luminosities at the highest redshifts. However, for all the data consistency arguments outlined above, we have good reason to suspect that when $\langle \beta \rangle$ in a given luminosity bin depends purely on low signal:noise
to relatively simple simulations. Specifically, we decided to insert into sources with the additional requirement of at least one 8–σ near-infrared detection. The final column simply gives the average value of β, further averaged over the redshift range \( z = 5 - 7 \), including values from each redshift bin where this is available. The data given here are plotted in Fig. 6.

5 SIMULATIONS

5.1 Simulation design

To explore and attempt to explain the origin of any apparent bias towards excessively blue values of β as derived from sources extracted with only \( \sim 4 - 5\sigma \) photometry, we undertook a set of relatively simple simulations. Specifically, we decided to insert into the ERS and HUDF HST (ACS+WFC3) and Spitzer IRAC images a population of galaxies at \( z \approx 7 \), with a chosen fixed intrinsic value of β, and then reclared these sources using exactly the same methodology as used to extract and refine the real high-redshift galaxy sample (i.e., including initial use of SExtractor, full ACS+WFC3-IRAC photometry from the real images, derivation of \( \chi^2 \) versus \( z_{\text{phot}} \), high-redshift sample refinement requiring a statistically acceptable solution at \( z_{\text{phot}} > 6 \), and final branding as ROBUST or UNCLEAR depending on whether \( \Delta \chi^2 > 4 \) between the low-redshift and high-redshift solutions).

We created three simulations, one in which all galaxies were assigned template SEDs with \( \beta = -2 \), one with all galaxies having \( \beta = -2.5 \), and an extreme simulation with \( \beta = -3.0 \). Perhaps the key feature of our simulations is that we inserted a galaxy population which extended substantially below the nominal flux limits of the images, following the form of the McLure et al. (2010) \( z \approx 7 \) luminosity function down to \( J_{125} = 30 \) (AB). This is vital to properly simulate the effect of “flux-boosting” of some subset of the numerous faint sources into the final galaxy sample. The point here is that, while completely erroneous 5-σ sources are extremely unlikely, the random flux boosting of, for example, 3-σ sources to \( \sim 5\sigma \) in either \( J_{125} \) or \( H_{160} \) can be relatively common when extracting a flux-limited sample down to the \( \sim 4 - 5\sigma \) limit in the presence of steep number counts. Moreover, such flux boosting is highly likely to be accompanied by a significant distortion in derived colour, in excess of that “expected” from adding the formal photometry errors in quadrature (because it is extremely unlikely that a source would fall on, for example, a 2-σ positive noise peak in both the \( J_{125} \) and \( H_{160} \) images).

| \( M_{UV} \) | \( \langle \beta \rangle \), \( z = 5 \) | \( \langle \beta \rangle \), \( z = 6 \) | \( \langle \beta \rangle \), \( z = 7 \) | \( \langle \langle \beta \rangle \rangle \) |
|---|---|---|---|---|
| -21.5 | -2.07±0.09 | -2.07±0.09 | -2.07±0.09 | -2.07±0.09 |
| -20.5 | -2.22±0.12 | -2.10±0.16 | -1.74±0.21 | -2.02±0.10 |
| -19.5 | -1.99±0.11 | -1.89±0.19 | -2.12±0.13 | -2.00±0.09 |
| -18.5 | -2.39±0.20 | -1.88±0.27 | -2.14±0.16 | -2.14±0.16 |

Figure 6. The upper panel shows final average \( \langle \beta \rangle \) versus UV absolute magnitude, \( M_{1500} \), at redshift \( z \approx 5 \) (blue), \( z \approx 6 \) (green), and \( z \approx 7 \) (red). Values, along with standard errors in the mean, are plotted for any redshift/luminosity bin where the quality control described in the text left more than one source. The lower panel simply shows the average of the data-points shown in the upper panel, and thus provides an average value of \( \beta \) for each luminosity bin, over the redshift range \( z = 5 - 7 \), including values from each redshift bin where this is available. These data are tabulated in Table 1. There is no clear evidence for any trend with either luminosity or redshift, and all values are consistent with \( \beta = -2 \).

5.2 Simulation results

We created many realizations for both the ERS and HUDF fields. A typical outcome is shown in Fig. 7, for both the \( \beta = -2 \) and \( \beta = -2.5 \) input catalogues. As in the earlier figures, ERS “sources” are indicated in red, HUDF “sources” in blue, and ROBUST and UNCLEAR high-redshift galaxies are indicated by solid and open symbols respectively.

While comparison with the earlier figures is complicated by the fact that Figs 1-3 include galaxies over the redshift range \( z = 5 - 8 \), and inevitably contain some genuine low-redshift inter-
monotonic luminosity dependence of $\beta = \text{given in Fig. 6 of Finkelstein et al. (2010). Here the analysis of our points plotted in Fig. 1 of Bouwens et al. (2010b), and to those shown in Fig. 8, again for both the $\beta$ contains some less significant detections which can bias the result that, with the depth of WFC3/IR data analysed here, unless such quality control is applied, a true measurement of $\beta$ with a true input value of $\beta$ has been successfully retrieved.

It is important to stress that the fact we recover $\langle \beta \rangle \approx -2.4$ at $M_{UV} \approx -19.5$ does not contradict the value of $\langle \beta \rangle \approx -2.12$ we measured from the $z = 7$ data in this bin, as given in Fig. 6 and Table 1. As already discussed, to try to minimize bias, these measurements were limited to objects with at least one > 8-$\sigma$ detection in the near-infrared, and even the $M_{UV} \approx -19.5$ luminosity bin contains some less significant detections which can bias the result to the blue unless filtered out. Thus, our simulation simply implies that, with the depth of WFC3/IR data analysed here, unless such quality control is applied, a true $\beta \approx -2$ will result in an accurately measured $\langle \beta \rangle = -2$ at $M_{UV} \approx -20.5$, a somewhat biased measurement of $\langle \beta \rangle \approx -2.4$ at $M_{UV} \approx -19.5$, and a severely biased measurement of $\langle \beta \rangle \approx -3$ at $M_{UV} \approx -18.5$. Thus, our simulation suggests that the apparent luminosity dependence of $\beta$ with $M_{UV}$ reported by both Bouwens et al. (2010b) and Finkelstein et al. (2010) (from the same depth of data) is at least not inconsistent with a true value of $\beta \approx -2$, independent of luminosity.

The lower panel in Fig. 8 simply shows how even bluer values, with apparent $\langle \beta \rangle < -3$, inevitably result when the input value of $\beta$ is $-2.5$. However, this is clearly inconsistent with the data, as the input value of $\beta = -2.5$ is of course correctly recovered from the simulation in the brightest luminosity bin, and this is inconsistent with the observed value of $\beta = -2$ at $M_{UV} = -20.5$.

Interestingly, the retrieved value of $\langle \beta \rangle$ in the faintest luminosity bin is not the full 0.5 lower in the lower panel of Fig. 8 as compared to the upper panel. This implies that one cannot easily correct for the bias in a unique way, and that a measured value of $\langle \beta \rangle \approx -3$ in this luminosity bin could be consistent with a true $\beta = -2$ or $\beta = -2.5$ within the errors. This simply reinforces the need to improve the depth of the WFC3/IR data to enable higher signal:noise measurements of $\beta$ in this crucial faint luminosity bin at $z \approx 7$.

5.3 The origin of “$\beta$ bias”

To explore the origin of the “$\beta$” bias so clearly displayed by the analysis of our simulations, we take advantage of the fact that the “true” input UV luminosity of every simulated galaxy is known, and explore how derived $\beta$ relates to the level of “flux-boosting” experienced by the simulated sources. This is shown in Fig. 9, where the extracted $\beta$ value for all of the reclaimed ERS and HUDF high-redshift $\beta = -2$ simulated galaxies is plotted against UV luminosity ($\equiv J$-band) flux boost, in magnitudes (here, a positive value of “Boost” means the reclaimed $J_{125}$ magnitude is brighter than the input value by the plotted magnitude difference).

Both the ERS and HUDF simulated galaxies behave in the same way and show that the extremely blue values of $\beta$ almost all result from sources which have entered the sample because their...
The UV slopes of high-redshift galaxies

Figure 8. Plots of average $\langle \beta \rangle$ versus UV absolute magnitude, $M_{1500}$, deduced from the individual $\beta$ values shown in Fig. 9 as reclaimed for the two alternative simulated $z \simeq 7$ galaxy populations. The upper plot shows how, without careful quality control, a galaxy population with a true value of $\beta = -2$, independent of $M_{1500}$ yields an apparent luminosity dependent average value of $\langle \beta \rangle$ which tends to $\langle \beta \rangle \simeq -3$ in the faintest luminosity bin from which sources can be selected in the current WFC3/IR HUDF data. The similarity between this plot and that presented by Bouwens et al. (2010b) (their Fig. 1) and by Finkelstein et al. (2010) (their Fig. 6) is striking. The lower plot shows the same information for the simulated $\beta = -2.5$ population. In both plots the correct value of $\langle \beta \rangle$ is only reclaimed in the brightest bin, and $\langle \beta \rangle$ becomes progressively more biased to the blue with decreasing luminosity.

“true” $J_{125}$ magnitudes have been boosted by a few tenths of a magnitude (up to $\simeq 0.5$ magnitudes). This is not really surprising - at the faintest limit a substantial fraction of the supposedly 5-$\sigma$ sources in the $J_{125}$ image are significantly flux boosted, and random noise dictates that these same sources are unlikely to be as extremely flux-boosted at $H_{160}$. Equation (1) indicates that a $J_{125}$ flux boost of 0.5 mag, will lead $\beta = -2$ to be distorted to $\beta = -4.2$, explaining naturally the behaviour displayed in Fig. 9.

However, what is less clear is why comparable flux-boosting in $H_{160}$ has not produced a comparable population of artificially red objects extending to $\beta > 0$. Unless the sample is specifically $J$-band selected there is no obvious reason why $J_{125}$ flux boosting should be more prevalent than $H_{160}$ flux boosting. The answer to this is rather subtle. $H$-band flux boosting does occur, and it can be seen that some sources do indeed have their $\beta$ values over-estimated, up to values approaching $\beta = 0$. However, when large/ red values of $\beta$ are produced by the noise and flux boosting, a significant fraction of the sources start to be classified as low-redshift sources by our code, and hence do not appear in Fig. 9 (which only contains objects with acceptable reclaimed solutions at $z_{\text{phot}} > 6$). Even among those “red” sources that do survive, with apparent $\beta \simeq -1$, it can be seen that few are classified as robust, simply because the measured redder $J - H$ colour permits an acceptable low-redshift solution.

In summary, as the scatter inevitably rises in the final luminosity bin, and is exacerbated by the effects of flux-boosting of fainter sources into the (apparently) flux-limited sample, the process of high-redshift galaxy selection can clip the red wing of the scattered values, and bias the average $\langle \beta \rangle$ value to the blue. This effect is not really specific to our particular method of source selection - a source scattered by $H_{160}$ flux boosting to $\beta > 0$ will have an apparent colour $J - H > 0.5$, and is therefore less likely to be regarded as a secure high-redshift source as selected by standard Lyman-break colour selection techniques. By contrast, any artificially “blue” galaxy resulting from $J_{125}$ flux boosting will almost always be retained, and indeed is liable to be classified as ROBUST.
We can of course check the extent to which this has happened in our simulated galaxy samples. Indeed, for the HUDF simulation shown in Figs 7–9, we find that from an input sample of 82 $z = 7$ galaxies, 12 were scattered out of the sample to low redshift due, in most cases, to their redder $J - H$ colours.

Finally, for completeness, we show in Fig. 10 the effect of restricting our analysis of the $z = 7$, $\beta = -2$ simulation to sources with at least one $> 8$-$\sigma$ detection with WFC3/IR, in effect replicating our final analysis of the real data as presented in Fig. 6. As with the real data, applying this level of quality control leaves us unable to say anything about $\beta$ at $M_{UV} \simeq -18.5$, but interestingly (and reassuringly) it also reduces the level of bias in the $M_{UV} \simeq -19.5$ luminosity bin to $\delta \beta \simeq 0.2$. Clearly the results presented in Fig. 6 are completely consistent with $\beta = -2$.

6 DISCUSSION

Our key results can be summarized as follows.

First we find that, at $z = 5$ and $z = 6$, the average value of UV slope is perfectly consistent with $\beta = -2$ and displays no significant luminosity dependence over the UV luminosity range $-22 < M_{1500} < -18$. Second, we find that the same result appears to hold at $z \simeq 7$, over the more restricted luminosity range $-21 < M_{1500} < -19$, but conclude that no robust statement can yet be made about $\langle \beta \rangle$ at fainter luminosities at $z > 6.5$. Third, we show, both via data consistency arguments from fields of varying depth, and from simple (yet realistic, and end-to-end) simulations that attempting to extend the measurement of average UV slope into the faintest available luminosity bin (as determined by $\simeq 4 - 5$-$\sigma$ detections) yields values of $\langle \beta \rangle$ which are biased to the blue, and can yield apparent average values as low as $\langle \beta \rangle \simeq -3$, even for a true input value of $\beta = -2$ for every source.

Thus, while we cannot rule out the recent claims that the faintest galaxies yet discovered at $z \simeq 7$ have extremely blue slopes, $\langle \beta \rangle \simeq -3$, we do show that such extreme values of $\langle \beta \rangle$ are not found (from the current data) in any luminosity or redshift bin where good-quality photometry is available (where “good” here means at least one detection in a WFC3/IR band at a significance level better than 8-$\sigma$). We note here that Finkelstein et al. (2010), while reporting raw results on $\langle \beta \rangle$ at $z = 5, 7$ (their Fig. 6) very similar to those reported by Bouwens et al. (2010b), derive larger errors on $\langle \beta \rangle$, and conclude that there is as yet no evidence for a dependence of $\langle \beta \rangle$ on $M_{UV}$ at $z \simeq 7$.

This, then, provides a very strong and clear motivation for still deeper WFC3/IR imaging in the HUDF, given the importance of testing the astrophysically important possibility that the very faintest high-redshift galaxies do display UV slopes significantly bluer that $\langle \beta \rangle = -2.5$, with all the associated implications for metallicity, age and ionizing photon escape fraction (Bouwens et al. 2010b; Robertson et al. 2010). A depth improvement of $\simeq 0.5$ mag. would be sufficient to convert most of the current $\simeq 5$-$\sigma$ detections to $\simeq 8$-$\sigma$ detections, thus enabling proper exploration of $\langle \beta \rangle$ down to $M_{UV,AB} \simeq 18$ at $z \simeq 7$.

Because of its novelty, and potentially crucial implications for reionization, we have focussed most of the above discussion, and indeed our simulations, on the measurement of $\beta$ at $z \simeq 7$. However, it is also of interest to assess how our results at $z \simeq 6$ and $z \simeq 5$ measure up to previous studies of $\beta$ at these and also lower redshifts.

The most obvious point of comparison is the major study of UV continuum slope over the redshift range $2 < z < 6$ carried out by Bouwens et al. (2009). This work presented extremely good evidence for a luminosity dependence of $\beta$ at $z \simeq 2.5$ and $z \simeq 4$. We wish to stress that our failure to find any such luminosity dependence in $\beta$ at higher redshifts should not be taken as casting doubt on these results at lower redshift. In particular, the evidence presented by Bouwens et al. (2009) for a steady decrease in $\langle \beta \rangle$ over the luminosity range $-22 < M_{UV} < -17$ appears compelling, based as it is on very large samples of Lyman-break galaxies in which $\beta$ can be determined purely from the optical photometry (i.e. from HST ACS $i'775 - z850$ colour). However, this luminosity dependence takes the average value of UV slope from $\langle \beta \rangle \simeq -1.3$ at $M_{UV} = -22.2$ to $\langle \beta \rangle \simeq -1.9$ at $M_{UV} = -17.2$, and is attributed by Bouwens et al. (2009) as being primarily a result of decreasing dust obscuration with decreasing UV luminosity (see also Stark et al. 2010). Crucially, even at the faintest luminosities probed at $z \simeq 4$, the bluest value of $\langle \beta \rangle$ reported by Bouwens et al. (2009) is $\langle \beta \rangle = -2.03 \pm 0.04 \pm 0.15$.

It is by no means obvious that a decrease in dust content with increasing redshift should maintain the slope of the $\beta - M_{UV}$ relation, simply shifting it to more negative values of $\beta$. As already discussed here and elsewhere, it is relatively straightforward for ‘normal’, essentially dust-free stellar populations to produce $\beta = -2$, but the production of significantly bluer slopes requires different astrophysics in the form of very young, very low metallicity stellar populations, with low levels of nebular emission.

The results presented by Bouwens et al. (2009) on $\beta$ at $z \simeq 5$ and $z \simeq 6$ are inevitably much more uncertain than those at lower redshift, in part because they involved the use of NICMOS data in the measurement of $\beta$. Nevertheless, at the brighter end of the luminosity range probed, at $M_{UV} \simeq -20.5$, our more robust measure-
ments support the conclusion of Bouwens et al. (2009) that Lyman break galaxies are bluer at \( z \simeq 5 - 6 \) than at \( z \simeq 4 \), with \( \langle \beta \rangle \) having moved from \( \langle \beta \rangle = -1.5 \pm 0.15 \) at \( z \simeq 4 \) to \( \langle \beta \rangle = -2 \pm 0.20 \) (see our Fig. 6 and the values given in Table 4 of Bouwens et al. 2009).

There is thus no serious doubt that the brighter Lyman break galaxies have become significantly bluer with increasing redshift, and the idea that this change is primarily due to decreasing dust content gains support from the very low (generally negligible) values of \( A_V \) inferred from the best-fitting SED models at \( z > 6.5 \) deduced by McLure et al. (2011). Therefore the key question now is whether the \( \beta - M_{UV} \) relation essentially plateaus at \( \beta \simeq -2 \) at \( z > 5 \) due to the near absence of dust at all luminosities, or whether there is indeed evidence for a continuing dependence of \( \beta \) on \( M_{UV} \), albeit perhaps with a different slope. Our own results, as shown in Fig. 6, support the former scenario, but as already discussed, our analysis also emphasizes the vital importance of deeper WFC3/IR data to establish the true values of the typical UV slopes of the very faintest galaxies at \( z \simeq 7 \).

ACKNOWLEDGEMENTS

JSD acknowledges the support of the Royal Society via a Wolfson Research Merit award, and also the support of the European Research Council via the award of an Advanced Grant. RJM acknowledges the support of the Royal Society via a University Research Fellowship. BER is supported by a Hubble Fellowship grant, program number HST-HF-51262.01-A, provided by NASA from the Space Telescope Science Institute, which is operated by which is operated by the Association of Universities for Research in Astronomy, Inc, under NASA contract NAS5-26555. DPS, MC and LdR acknowledge the support of the UK Science & Technology Facilities Council via the award of a Post-Doctoral Fellowship, an Advanced Fellowship, and a Post-Doctoral Research Associate position respectively. This work is based in part on observations made with the NASA/ESA Hubble Space Telescope, which is operated by the Association of Universities for Research in Astronomy, Inc, under NASA contract NAS5-26555. This work is also based in part on observations made with the Spitzer Space Telescope, which is operated by the Jet Propulsion Laboratory, California Institute of Technology under NASA contract 1407.

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