Abstract—In this paper, we have proposed a novel algorithm for identifying the modulation scheme of an unknown incoming signal in order to mitigate the interference with primary user in Cognitive Radio systems, which is facilitated by using Automatic Modulation Classification (AMC) at the front end of Software Defined Radio (SDR). In this study, we used computer simulations of analog and digital modulations belonging to eleven classes. Spectral based features have been used as input features for Sequential Minimal Optimization (SMO). These features of primary users are stored in the database, then it matches the unknown signal’s features with those in the database. Built upon recently proposed AMC, our new database approach inherits the benefits of SMO based approach and makes it much more time efficient in classifying an unknown signal, especially in the case of multiple modulation schemes to overcome the issue of intense computations in constructing features. In various applications, primary users own frequent wireless transmissions having limited their feature size and save few computations. The SMO based classification methodology proves to be over 99 % accurate for SNR of 15 dB and accuracy of classification is over 95 % for low SNRs around 5dB.

Keywords—Automatic modulation classification, cognitive radio, Database, sequential minimal optimization, unknown signal detection, primary user, spectral based features.

I. INTRODUCTION

Cognitive Radio (CR) is a cutting edge technology on which rigorous research and Development (R&D) is occurring recently. CR enables efficient usage of radio frequency spectrum. Empty spaces in both licensed and unlicensed spectrum, commonly known as white spaces are used by CR to achieve its set of objectives. The idea here is to sense for a spectrum hole and use it until its rightful owner appears. The CR then modifies its frequency to match another white space and possibly another class of modulation scheme and coding. This phenomenon supposedly may occur every now and then, imposing a heavy feedback to the receiver every time the modulation scheme and the coding changes. One possible solution to this problem is to use Digital Signal processing (DSP) analysis called automatic modulation classification. These calculations can determine the type of modulation effectively using particular feature set. But most of the work in this direction is applied to High Frequency (HF) noise and cannot be applied to Additive White Gaussian Noise (AWGN) channels. [1]

The goal of this study is to implement an automatic modulation classifier in an AWGN environment. So, we designed the database assisted AMC, analysed the need for fast classification and proposed a solution. This paper proposes Sequential Minimal Optimization (SMO) to train the Support vector machines (SVMs) to do classification by segregating a mixture of both digital and analog modulation schemes into different classes. Consequently, our contribution to Cognitive Radio research lies in classifying an unknown signal in a time efficient manner, through integration of database.

The paper is organized as follows: Section II explains sequential minimal optimization and related work. Simulation of modulated signals, feature extraction and modulation classification are presented in Section III. Section IV is about proposed database assisted design and algorithm. Results and discussions of proposed approach are presented in Section V. Conclusion is drawn in VI.

II. SEQUENTIAL MINIMAL OPTIMIZATION

In recent years, there has been shown a lot of interest by researchers in application of Support Vector Machines (SVMs), as they perform well on a wide variety of problems related to pattern recognition. But, there are some drawbacks in SVMs, due to which it is not widely used by large research communities. First reason is that training SVMs is slow, especially for large problems. Second explanation is that they are complex, subtle, and can be implemented by an expert engineer.

SMO is widely used in training support vector machines (SVMs). The amount of memory required for this algorithm is linear in the training set size, due to which large training sets are handled with very less complexity and also matrix computation is avoided. So, SMO spans somewhere between linear and quadratic in the training set size for various test problems, while the standard SVM algorithm spans somewhere between linear and cubic in the training set size. SMO’s computation time is took over by SVM evaluation, hence SMO is the best algorithm for linear SVMs. On real world sparse data sets,
SMO can be approximately more than 1000 times faster than the normal algorithm [2].

An SMO model is a representation of the data sets as points in space. They are mapped so that the data sets of the separate categories are divided by a clear gap, which is as wide as possible. New data sets are then mapped into that same space and predicted to belong to a category based on which side of the gap they fall into. It trains a support vector classifier using kernel functions such as Gaussian and Polynomial kernels and takes minimal time in doing so [2].

The $K(x, x_i)$ are the support vectors used by SMO. $\alpha$ is the weight or lagrange multiplier. The output equation is given as,

$$y = f(x); f(x) = \sum_{k=1}^{m} \alpha_k K(x, x_k) + b$$  \hspace{1cm} (1)

A. Related works

Azzouz and Nandi [3] have proposed spectral based features and algorithms to classify both analog and digital modulated signals. Popoola and Olse have extracted same set of features and proposed ANN based classification system [4]. The key features proposed by Nandi are later used in [5] [6] and many more. But in practicality, accuracy of these features depends upon noise, carrier offset error, symbol rate estimation error that affect the probability of identification. Arulampalam et al., [13] have used only digital modulation schemes using ANN and features proposed by Nandi and Azzouz, validated over non-weak segment of the incepted signal and also used maximum power spectral density of normalized instantaneous frequency of intercepted signal. When we compare our work with the study, we have obtained better results by using SMO Algorithm [8] [15] for classification of both analog and digital modulations at low SNRs. Our contribution is in building upon this existing work on AMC, via a database approach and classifying the unknown signal in a time efficient manner.

III. STUDY METHODOLOGY

The study flow involved three steps. The first step was extraction of the statistical features keys used as inputs to the developed classifier. The second step was development of automatic modulation classifier system. Third step was to integrate the system with the database. Satisfactory accuracy was achieved in the final step.

A. Simulation of modulated signals

Signals are generated for eleven modulation schemes, which includes both analog and digital modulations. Modulated signals are generated using the formulas. For example, the AM modulated signal is generated using the formula,

$$Y_{am}(t) = [1 + K_a, F_i](\cos(2\pi f_s t))$$  \hspace{1cm} (2)

The FM modulated signal is generated using the formula,

$$Y_{fm}(t) = \cos(2\pi f_s t + k_f \sin(2\pi f_m t))$$  \hspace{1cm} (3)

Similarly DSB, SSB, ASK, FSK and PSK modulated signals in an AWGN environment were generated in MATLAB using standard formulas.

B. Feature extraction

Feature extraction is a prerequisite for recognition. The motive here is to identify a pattern by using minimum number of features or attributes, which are important for determining the pattern class identification. The employed classification technique was derived from the amplitude, phase and frequency instantaneous values of signal simulations. These values are obtained from the discrete time analytic signal. Hilbert transform is used for calculating the instantaneous values of a signal. The key features used in this paper are spectral based features and had earlier been used by Nandi [3] [7].

(i) $\gamma_{max}$ : This feature corresponds to maximum value of the PSD (Power spectral density) . It measures the variance in signal amplitude.

$$\gamma_{max} = \frac{\max_{DFT(a_cn[n])^2}}{N}$$  \hspace{1cm} (4)

i.e. taking a discrete Fourier transform of the signal samples. Here $a_{cn}(n)$ is centered instantaneous amplitude at time, $t = \frac{n}{f_s} (n = 1, 2, 3...N)$ and a sampling frequency, $f_s$. $a_{cn}(n)$ is defined as

$$a_{cn}(n) = a_n[n] - 1 , a_n(n) = \frac{a[n]}{m_a}$$  \hspace{1cm} (5)

Here $m_a$ is the mean value of samples.

$$m_a = \frac{1}{N} \sum_{n=1}^{N} a[n]$$  \hspace{1cm} (6)

All centered values refer to normalized instantaneous values.

(ii) $\sigma_{dp}$ : This feature measures the variance in direct instantaneous phase. It discriminated 2PSK from other modulation schemes. This is given as $\sigma_{dp}$

$$\sigma_{dp} = \sqrt{\frac{1}{N} \left( \sum_{n=1}^{N} A_{n} > A_{i} \Phi_{NL}^2[n] \right) - \left( \frac{1}{N_c} \sum_{n=1}^{N_c} A_{n} > A_{i} \Phi_{NL}^2[n] \right)^2}$$  \hspace{1cm} (7)

(iii) $\sigma_{ap}$ : This feature corresponds to the standard deviation of the centered non-linear component of the instantaneous phase. Here we take absolute values. This is given as $\sigma_{ap}$

$$\sigma_{ap} = \sqrt{\frac{1}{N_c} \left( \sum_{n=1}^{N_c} A_{n} > A_{i} \Phi_{NL}^2[n] \right) - \left( \frac{1}{N_c} \sum_{n=1}^{N_c} A_{n} > A_{i} \Phi_{NL}^2[n] \right)^2}$$  \hspace{1cm} (8)

This is very useful in finding PSK modulation order.

(iv) $P$ : This feature is the calculation of spectrum symmetry around the carrier frequency. This quantity is a decision factor to classify amplitude-based modulations with different properties in the frequency domain.

$$P = \frac{P_s - P_o}{P_s + P_o}$$  \hspace{1cm} (9)

$P_s$ is the spectral power of sideband (lower) and $P_o$ is the spectral power of the other sideband (upper).

$$P_s = \sum_{n=1}^{f_{cn}} |F(n)|^2 , P_o = \sum_{n=1}^{f_{cn}} |F[n + f_{cn} + 1]|^2$$  \hspace{1cm} (10)

Here $F(n)$ is the Fourier transform of the received signal. $(f_{cn} + 1)$ is the sample number for carrier frequency $f_c$ , $f_{cn}$ is defined as

$$f_{cn} = \frac{f_c}{f_s} - 1$$  \hspace{1cm} (11)
(v) \( \sigma_{aa} \): This feature corresponds to the standard deviation of the centered instantaneous amplitude of signal samples. \( N \) is the total number of signal samples. We take absolute and normalized values. Though this feature is similar to \( \gamma_{max} \), it has the ability to discriminate 2ASK from other modulation schemes.

\[
\sigma_{aa} = \sqrt{\frac{1}{N} \left( \sum_{n=1}^{N} A_{cn}^2(n) \right) - \left( \frac{1}{N} \sum_{n=1}^{N} |A_{cn}(n)| \right)^2} \tag{12}
\]

(vi) \( \sigma_{af} \): This feature corresponds to standard deviation of the centered frequency. We take absolute and normalized values. It has the ability to discriminate 2ASK from 4ASK. \( N_c \) is the number of samples that meet the condition: \( A_{n}[n] > A_t \). \( A_t \) is the threshold value.

\[
\sigma_{af} = \sqrt{\frac{1}{N_c} \left( \sum_{A_{n}[n]>A_t} f_{N}^2(n) \right) - \left( \frac{1}{N_c} \sum_{A_{n}[n]>A_t} |f(n)| \right)^2} \tag{13}
\]

(vii) \( \sigma_a \): This feature corresponds to the standard deviation of the centered frequency. We take normalized values here. It has the ability to differentiate 2ASK and 4ASK.

\[
\sigma_a = \sqrt{\frac{1}{N_c} \left( \sum_{A_{n}[n]>A_t} \sigma_{cn}^2[n] \right) - \left( \frac{1}{N_c} \sum_{A_{n}[n]>A_t} a_{cn}[n] \right)^2} \tag{14}
\]

(viii) \( \mu_{42}^{a} \): This feature is the kurtosis of normalized and centered instantaneous amplitude. It differentiates AM signal from the rest.

\[
\mu_{42}^{a} = \frac{E[A_{n}^4[n]]}{(E[A_{n}^2[n]])^2} \tag{15}
\]

(ix) \( \mu_{42}^{f} \): This feature is the kurtosis of normalized and centered instantaneous frequency. It differentiates FM signal from the rest.

\[
\mu_{42}^{f} = \frac{E[f_{N}^4[n]]}{(E[f_{N}^2[n]])^2} \tag{16}
\]

C. Modulation classification

Modulation can be defined as varying amplitude, frequency and phase of a carrier wave with frequency \( f_c \) with respect to modulating signal with frequency \( f_m \) [6].

While training the SVM, nominal attributes in the arff format are converted into two class (binary) ones. Coefficients in the output are based on the normalized data. The SMO algorithm will use pair wise classification considering the fact that the problem here is a multi-class one. We choose to make use of Poly Kernel i.e. polynomial kernels. Here since we have 11 classes the 11 binary SMO models have been output with one hyperplane each to support each of the possible pair of class values. In such Kernel based methods, similarity must be a kernel function satisfying some mathematical properties [11] [12].

IV. DESIGN AND ALGORITHM

The steps in design of the database assisted AMC are presented in Fig. 1.

The steps for implementing the Database assisted AMC system are divided into two phases.

1) Offline Phase:
- Firstly we had realized computer simulated signals of different modulation schemes using MATLAB codes reproducing the work of A.K. Nandi and E.E. Azzouz [3].
- Then, stored the simulated and labeled signal data into the database server.
- Thereafter we have generated reference sample data, to train the SMO model offline.
- Further saved the trained model into the file system.
- Thereafter we had generated computer simulated signals of different modulation schemes using MATLAB codes reproducing the work of A.K. Nandi and E.E. Azzouz [3].
- Then, stored the simulated and labeled signal data into the database server.

2) Classification Phase:
- Secondly we have connected to the database using JDBC MySQL connector/J.
- Accordingly fetched all the unlabeled data into the program.
- Next we attached arff (attribute relation file header) header format to this data in order to transform it into an arff test file.
- Then read the testing file into the program and loaded the trained SMO model.
- Afterwards we have applied the model’s configuration on the test file. With this step, modulation classification is completed. In the end, updated the database server with the classified signal data.

V. RESULTS AND DISCUSSIONS

Here we have input test data (unknown signal) of 25dB SNR and applied an SMO trained model over it. The model uses...
In database assisted approach, when an unknown signal’s features are among the training data stored in database, an existing record in the database is selected and its modulation scheme is returned. We have first trained the SMO classifier and stored the trained model in WEKA [9] and database. Finally, we are classifying unknown signal with an assumption that it should belong to one of the known modulation schemes mentioned in section III of this paper.

In our database assisted approach, we record the features of known signals in the database system. Then, AMC monitors each incoming signal’s transmitting sequence. For example, let us suppose that initially only one known signal, such as AM is present in an environment and detect the unknown signal. Then, in the next input sequence consider only two known signals such as AM, FM and compare the unknown signal’s feature vectors with those in the database. In various applications, known signals have routine wireless transmissions, hence they own a limited number of feature vectors, meaning that the subsequent database is stable and limited in size. Whenever an unknown signal’s feature vector does not have a match entity in the database, our approach will detect it’s action as unusual by taking the stability of known signals into account and identifies it as a malicious signal, hence save some computations compared to the previous approaches in the literature. This way we realized that our proposed idea on database assisted approach for AMC is a novel work. So, we ran computer simulations and in future would like to implement this idea on a system model similar to cognitive radio scenario of known signals. Known signals are analogous to primary users’ signals and an unknown signal referred as primary user is to be detected so that interference can be avoided with neighboring primary users. Therefore, we assumed all basic modulation schemes possible as the only modulation types used by authentic primary users’ signals, referred as known signals. Here our research contribution is to evaluate the performance of database approach over non database in terms of efficiency, thereby solving the problem of severe computations in constructing features.

Our limitations are as follows:

1) At any instance of time, only one signal is transmitted by user’s either primary, unknown or secondary.
2) Secondary user’s transmit at very low powers not interfering with primary and unknown users.
3) Secondary users, unknown users and primary users are utilizing the area within the same frequency band.
4) Secondary user’s modulation scheme is different from primary and unknown users.
5) We cannot detect intelligent unknown user’s who pretend to be primary users.
6) We have not considered other modulation schemes for transmission of unknown signal, instead used only those modulation schemes mentioned in section III of this paper.

In non database approach, we have assumed that the test signal’s feature is among the training data. To match this test signal to a record in the arff format, we need to search for the record. But running a search query is not preferred in flat files (File that doesn’t have any internal hierarchy). The reason is that database is a structured way of storing data, whereas flat file is unstructured way of storing data.

It is very clear from Fig. 2 that for both database and non database methods the time taken for classifying an unknown signal is surely dependent on number of known signals. When there are more known signals in the system, it consumes more time for conclusion. However, it is observed that with a larger number of known signals, the classification time increases more drastically in the case of non database approach. The database assisted approach takes linear growth, because time taken for classification is dominated only by searching time of database. Whereas, non database approach follows approximately exponential rise, due to increase in classification time with number of known signals.

At low SNRs like 5 dB, as signals are transmitted with low power, it is a challenge to classify 11 different modulation schemes, as sometimes there is confusion to classify the similar modulation schemes. Generally, we get accuracy of 80-90% at low SNRs by recent methods. But by these features we are getting around 95%.

A. Probability of correct detection

In multi-class prediction, the result on a test set is often displayed as a two dimensional confusion matrix with a row and column for each class. It is defined by this formula, 
\[ P = \frac{TP + TN}{TP + TN + FP + FN} \]. Here TP means True Positives, TN means True negatives, FP means False positive and FN means False negative. The error rate is one minus this [10].
Table I illustrates the improvement of present work with reference work by Popoola’s [4] feed forward neural networks [14]. Table II and III illustrate the confusion matrix for different modulation schemes at an SNR = 15 dB.

VI. CONCLUSION

In this paper, we have developed and implemented an AMC with database acting as an abettor in automating the whole process of classification. The database assisted approach gave us better results than the non database approach in terms of time taken. We have applied SMO model configuration on both labeled and unlabeled data. Firstly, SMO based classification alone gave better performance when trained and evaluated with labeled signals. The results proved to be over 98% accurate for 15 dB data. The future work of this paper includes validation of our approach through hardware implementation to show its feasibility in real life conditions.

In future, we will also consider same modulation type during classification. Till now we are assuming that the unknown signal’s modulation should belong to any one of the 11 modulation schemes generated in simulations. But, in real life we need to detect an unknown signal, which may be different from modulations stored in database. Then, we consider such an unknown signal as malicious. Now, as malicious users (unknown users) are intelligent, they pretend modulations of primary users. So, in this case, if both primary and unknown users use same modulation type, and no match is found in database. Then, during the detection phase of unknown signals, one can employ a new method, which will detect these type of unknown signals.