Damping ratio analysis of tooth stability under various simulated degrees of vertical alveolar bone loss and different root types

Kuo-Ning Ho¹, Sheng-Yang Lee¹*† and Haw-Ming Huang¹,²*†

Abstract

Background: The purpose of this study was to evaluate the feasibility of using damping ratio (DR) analysis combined with resonance frequency (RF) and periotest (PTV) analyses to provide additional information about natural tooth stability under various simulated degrees of alveolar vertical bone loss and various root types.

Methods: Three experimental tooth models, including upper central incisor, upper first premolar, and upper first molar were fabricated using Ti6Al4V alloy. In the tooth models, the periodontal ligament and alveolar bone were simulated using a soft lining material and gypsum, respectively. Various degrees of vertical bone loss were simulated by decreasing the surrounding bone level apically from the cementoenamel junction in 2-mm steps incrementally downward for 10 mm. A commercially available RF analyzer was used to measure the RF and DR of impulse-forced vibrations on the tooth models.

Results: The results showed that DRs increased as alveolar vertical bone height decreased and had high coefficients of determination in the linear regression analysis. The damping ratio of the central incisor model without a simulated periodontal ligament were 11.95 ± 1.92 and 27.50 ± 0.67% respectively when their bone levels were set at 2 and 10 mm apically from the cementoenamel junction. These values significantly changed to 28.85 ± 2.54% (p = 0.000) and 51.25 ± 4.78% (p = 0.003) when the tooth model was covered with simulated periodontal ligament. Moreover, teeth with different root types showed different DR and RF patterns. Teeth with multiple roots had lower DRs than teeth with single roots.

Conclusion: Damping ratio analysis combined with PTV and RF analysis provides more useful information on the assessment of changes in vertical alveolar bone loss than PTV or RF analysis alone.

Keywords: Resonance frequency, Damping ratio, Tooth, Stability
Radiographic analysis is another useful method for evaluating the quantity and quality of periodontal conditions, but a limitation of this method for diagnosing periodontal conditions is its low resolution. It is difficult to detect the bone status at the periodontal interface when demineralization is less than 30% [4, 5]. Since there is a strong correlation between the degree of tooth mobility and the loss of alveolar bone [6], measurement of tooth mobility can be used as a diagnostic parameter in evaluating periodontal tissue conditions.

The periotest (Siemens AG, Bensheim, Germany) was introduced as the first diagnostic device that measures tooth mobility objectively. The periotest can be used to detect not only tooth movement but also the early stages of ankyloses caused by dental trauma [7]. The device uses contact times between an acceleration rod and the target tooth surface as a parameter to represent the tooth mobility [8–10]. However, several investigators report that the periotest results do not always correspond precisely to biomechanical parameters because the periotest values (PTVs) are strongly related to the excitation direction, application force, and position [1, 11–13]. Recently, Goellner et al. detected teeth mobility of healthy individuals by both the periotest and a quantitative metric tooth mobility measuring method. They found no correlation between the metric displacement of the tooth and PTVs [14]. They suggested that besides the tooth displacement, the properties of the periodontal ligament also influence the PTV.

To overcome this problem, several researchers have tried to develop new techniques to analyze tooth mobility and periodontal tissue condition using different mechanical parameters. The resonance frequency is a vibrational parameter. Mathematically, the resonance frequency is a function of the stiffness and mass of a structure and is related to the boundary conditions of a vibrating object [15, 16]. In implant dentistry, the resonance frequency is also a useful diagnostic tool in the assessment of dental implant stability [17–20]. Lee et al. calculated the resonance frequencies of healthy upper central incisors using the finite element method and indicated that the resonance frequency was lower when the surrounding bone was decreased horizontally [21]. Based on this finding, Huang and colleagues measured the resonance frequencies of the anterior teeth in vivo [15, 16]. They found that the mean resonance frequencies of anterior teeth significantly decreased when periodontium attachment loss was greater than 4 mm. These findings suggest that resonance frequencies could be a useful parameter for assessing periodontal conditions clinically, such as the root length in alveolar bone [19] and molar furcation involvement [22]. However, until now, no resonance frequency device for detecting periodontal clinical conditions was commercially available. One possible reason for this lack of availability could be the low sensitivity of resonance frequency measurements for detecting periodontitis. In an in vivo study, Wang et al. showed that the difference in resonance frequencies between healthy teeth and teeth with periodontitis was only 6% [22].

The damping factor is another important parameter of vibration analysis. Damping is an effect that reduces the amplitude of vibrations in an oscillatory system. For nondestructive tests, damping is considered an important parameter for determining the viscoelastic behavior of composite materials by measuring energy loss. This loss of energy is known as the damping capacity [23]. In engineering, the damping effect can be expressed as the damping ratio, a dimensionless measure describing how oscillations of a structure decay after a disturbance. It is defined as the fraction of strain energy lost in
one full cycle of deformation. Recent studies have demonstrated that the damping can be used as a noninvasive tool for monitoring changes in bone properties [24, 25], discriminating between varying degrees of osteoporosis and bone fracture [26], and diagnosing osseointegration during the dental implant healing process [27–29].

The periodontal ligament is a soft, richly vascular and cellular connective tissue that surrounds the roots of the teeth and joins the root cementum with the alveolar bone [30]. This structure distributes and absorbs forces produced during mastication and other types of tooth contact into the alveolar process via the alveolar bone proper. Thus, the periodontal ligament tissue acts as a damping mechanism that assists in the absorption of occlusal forces around the alveolar region of a loaded tooth [31]. Nonetheless, a device for determining the periodontal condition that directly measures the damping properties of a tooth remains unavailable.

Since successful treatment is based on a thorough examination, evaluation of tooth stability is an important diagnostic process that contributes greatly to treatment planning and clinical management. The aim of this study was to test whether the damping ratio provides useful information on tooth stability as the boundary conditions are decreased in teeth with various root types.

Methods
In vitro model setup
To evaluate the influence of different root types on the detected damping ratios, three types of teeth models, including upper central incisor, upper first premolar, upper first molar, with simulated periodontal ligaments, were fabricated (Fig. 1a). The model teeth were made of Ti6Al4V (115 GPa, 3D Printer Products, Chinmintai, Taipei, Taiwan). The shapes of the model teeth were adopted from standard teeth (Nissin Dental Products Inc., Kyoto, Japan). According to previous studies, a tissue conditioner for soft lining material (0.38 MPa, Shofu Tissue Conditioner II, Shofu Inc., Kyoto, Japan), and gypsum (1.76 GPa, Heraeus Kulzer GmbH, Germany) were used to simulate the periodontal ligament and alveolar bone, respectively [1, 32]. The thickness of the periodontal ligament of the simulated tooth models was 0.25 mm [33]. It was prepared according to previous work [34]. Briefly, root surfaces were dipped into melted wax (GEO Dip, Renfert GmbH, Germany) up to 2–10 mm below the CEJ. The 0.25 mm thick wax layer was confirmed with digital calipers. The roots of the teeth were embedded in gypsomes in a plastic container (Fig. 1a). After gypsum set, the teeth were moved out from the gypsum and the wax was removed. Then tissue conditioner was used to fill the spaces between the simulated teeth and gypsoms.

Experimental procedures
In this study, a noninvasive impulse-forced vibrational method was used to determine the damping ratios of the tested teeth. As shown in Fig. 1b, the probe consisted of an impact rod and a piezoelectric microphone, as described previously [35]. When a current passed through an electromagnetic coil, the impact rod was driven forward by an electromagnetic force. In this study, central position on the tooth buccal surface was selected as impact point (Fig. 1a). The signal was detected by the microphone and sent to the spectrum analyzer (Implomate, Biotech One, Taipei, Taiwan). The frequency
response was calculated using Fast Fourier Transform software. The specific resonance frequency (Fn) of the simulated teeth was determined from the highest point with a peak value of the vibration amplitude. The damping ratio was calculated using the half-power method (Fig. 1c) from the following formula [25, 33, 36]:

\[
DR = \frac{(F_b - F_a)}{2F_n}
\]

where Fn is the resonance frequency, (Hz) and Fa and Fb are the frequencies obtained from the points at 0.707 times the maximum amplitude of the resonance frequency. The formula used to calculate the damping ratio was justified in several previous in vitro studies [25, 33, 37].

To evaluate the influence of the simulated periodontal ligament on the test parameters, the damping ratio, resonance frequency were measured with a novel analyzer (Imp- lomate, Biotech One, Taipei, Taiwan) which was described in previous research [29], and periotest (Siemens) were measured simultaneously [28] in conditions with various alveolar vertical bone loss in a tooth model with a single root (central incisor model) with and without a simulated periodontal ligament. In addition, the three parameters were measured in the three simulated teeth with various degrees of vertical bone loss simulated by decreasing the surrounding bone level apically from the cementoenamel junction in 2-mm steps incrementally downward for 10 mm [22, 38].

---

**Fig. 1** a The fabricated tooth models. The model setup with simulated tooth, periodontal ligament and alveolar bone. White arrows indicated the impact positions. b The detector probe consisted of a piezoelectric microphone and an impact rod, driven by electromagnetic coil. c The typical frequency response spectrum of the vibration experiment. Damping ratio was calculated using the half-power method. Fn, resonance frequency. Fa and Fb are the frequencies at 0.707 times the maximum amplitude of the resonance frequency.
Statistical analysis
Each measurement was obtained from three samples to verify its accuracy. The data are obtained from at least three separate measurements and are presented as means and standard deviations. A linear regression analysis was done to validate the detection technique and examine the relationships of the periotest value, RF, and the damping ratio in all tooth models with various simulated alveolar bone heights. Kruskal–Wallis and Dunn post hoc tests (SPSS, IBM) were used to assess the association between damping ratio and the conditions at the tooth-bone interface for various degrees of vertical bone height. p < 0.05 was considered to indicate statistical significance.

Results
Resonance frequency, PTV, and damping ratio of the upper central incisors with and without periodontal ligaments were determined to evaluate the influence of the simulated periodontal ligament on the test parameters. For the tooth model without a simulated periodontal ligament, the RF, PTV, and damping ratio of the model with a bone level at 2 mm apically from the cementoenamel junction were 3716.67 ± 160.73 Hz (Fig. 2a), −3.62 ± 0.30 (Fig. 2b) and 11.95 ± 1.92% (Fig. 2c), respectively. When the amount of vertical alveolar bone loss increased from 2 to 10 mm, the RF decreased to 1950.00 ± 91.29 Hz (Fig. 2a) while the PTV and damping ratio increased to 15.57 ± 0.99 (Fig. 2b) and 27.50 ± 0.67% (Fig. 2c), respectively. The presence of periodontal ligament tended to decrease the resonance frequency (p = 0.026 < 0.05) and increase the PTV (p = 1.46 × 10⁻⁵ < 0.05) and increase damping ratio (p = 2.14 × 10⁻¹⁰ < 0.05) of the tooth models. When the upper central incisor model was covered with simulated periodontal ligament and embedded in the same simulated surrounding tissues, the detected RF, PTV, and damping ratio at 2 mm were 2858.33 ± 78.62 Hz (Fig. 2a), −0.78 ± 0.13 (Fig. 2b), and 28.85 ± 2.54% (Fig. 2c), respectively. These values changed to 1700.00 ± 136.93 Hz (Fig. 2a), 32.50 ± 1.17 (Fig. 2b), and 51.25 ± 4.78% (Fig. 2c) when the simulated bone levels of the tooth models were set at 10 mm apically from the cementoenamel junction. The PTV and damping ratio data were plotted against the analogous resonance frequency data. As shown in Fig. 3a, poor correlation was found between PTV and resonance frequency (R² = 0.7984). However, a higher correlation coefficient was obtained between damping ratio and resonance frequency (R² = 0.9077) (Fig. 3b).

Figure 4 shows that regardless of the bone level, the upper first molar model had the highest resonance frequencies compared to the other two tooth models in all simulated bone loss situations. Among the three models, the upper central incisor exhibited the lowest resonance frequencies. For upper central incisor, upper first premolar, and upper first molar models, the fold changes in RF from 2 to 10 mm were 1.68, 1.86, and 1.87, respectively. For the periotests, the opposite trend was observed. The upper first molar showed the lowest PTV compared to the upper central incisor and upper first premolar models. A significant difference in PTV between the upper central incisor and upper first molar was observed only when the bone level was set at 10 mm apically from the cementoenamel junction (Fig. 5). The damping ratio showed a trend similar to the PTV. The damping ratio of the upper first premolar and the upper central incisor showed no significant difference (p > 0.05) when the bone level was changed from 2 to 10 mm downward from the cementoenamel junction (Fig. 6). The damping ratios at the 2-
4-mm bone levels were 15.46 and 22.15%, which were significantly lower than the damping ratios of the upper central incisor and the upper first premolar at the same bone levels (p < 0.05). For the upper central incisor, upper first premolar, and upper first molar, the fold changes in damping ratio from 2 to 10 mm were 1.77, 1.57, and 2.58, respectively.
The objective of this study was to evaluate and compare the correlation between tooth stability parameters, represented by PTV, resonance frequency and damping ratio. In addition, the damping ratio analysis for continuously monitoring the various degrees of vertical alveolar bone loss and different root types were also assessed. The resonance

![Graphs showing correlation between PTV, resonance frequency, and damping ratio.](image)

**Fig. 3** The relationship between the resonance frequency of the tested tooth model and the a periotest value and b damping ratio. A high correlation was found between the readings of resonance frequency and damping ratio.

![Graph showing changes in resonance frequencies with bone loss.](image)

**Fig. 4** Changes in the resonance frequencies of the models with various root types and degrees of bone loss. UCI upper central incisor, UFP upper first premolar, UFM upper first molar.

### Discussion

The objective of this study was to evaluate and compare the correlation between tooth stability parameters, represented by PTV, resonance frequency and damping ratio. In addition, the damping ratio analysis for continuously monitoring the various degrees of vertical alveolar bone loss and different root types were also assessed. The resonance
frequency is used for evaluating the stability of natural teeth [19, 21]. Huang et al. [15] found that the mean resonance frequency of anterior teeth significantly decreases in value due to tooth periodontal attachment loss. The results of our study showed that the resonance frequencies of the simulated teeth decreased with the simulated alveolar bone loss (Fig. 2a). This finding is consistent with previous in vivo data [15, 16, 21], which also showed that teeth with periodontal disease exhibited lower resonance frequencies compared to analog teeth with healthy attachment bone levels.

According to previous reports, the elastic modulus of enamel top surface measured between 101 and 117 GPa [39, 40]. Most metals that can be manufactured for 3D printing, such as Co-Cr alloy and stainless steel, have greater elastic moduli than enamel. With this regard, Ti6Al4V (115 GPa) was selected for fabricating the simulated teeth in this study. Since the real damping ratio of the teeth cannot be determined and the results presented above can only reflect the trend of changes in DF values.

In Fig. 4, the resonance frequencies of upper first molars samples are higher than that of upper first premolar and upper central incisor samples. The reason is that the first molar is a three-root tooth, which demonstrates greater stability than the other tooth models with one or two roots. A previous finite element analysis also indicated that RF curves of single-root teeth and multiple-root teeth showed decreasing trends with
alveolar bone height loss, and the multiple-root teeth had higher resonance frequencies than single-root teeth did at the same alveolar bone height [22, 38, 41].

The periotest (Siemens) is reported to be an accurate detector for measuring tooth mobility and is used in the diagnostic evaluation of periodontal disease. The PTV is a measure of the displacement amplitude of a tooth upon subjection to an impact loading. For years, the PTV was used to represent the periodontal ligament of the target tooth [14, 42]. Feng et al. utilized resonance frequency and damping ratio in dental implant study and found that when the Young’s modulus of the surrounding bone increased, the implant resonance frequency increased and the damping ratio and PTV values decreased [27–29]. This negative correction phenomenon between the resonance frequency and damping property was also observed in our study (Fig. 3). Molar furcation involvement is an important factor in both biomechanical and clinical periodontology [38]. As shown in Fig. 5, the upper first molar model exhibited lower PTV and damping ratio than other models did. Notably, when the amount of vertical alveolar bone loss increased from 4 to 6 mm apically from the cementoenamel junction, the PTV of the upper first molar model increased remarkably. This increase indicates that the multiple-root teeth had higher stability than single-root teeth, which confirms the findings reported by Doshi et al. [43].

When we evaluated the association of PTVs with the amount of bone and clinical attachment loss, the anterior teeth showed higher PTVs compared with the posterior teeth; and the mandibular teeth showed higher PTVs compared with the maxillary teeth. Interestingly, we also found that when alveolar bone loss exposed a furcation, the tooth stability decreased significantly (Fig. 5). We observed increasingly greater loss of stability with the number of furcations exposed. Generally, trifurcated upper first molars had the best stability, followed by bifurcated upper first premolars, and then furcation less upper central incisors.

Damping property is a phenomenon to describe how oscillations in a system decay after a disturbance. The load response of the viscoelastic tissues can be strain-rate dependent. Since the more is the hysteresis in the stress–strain curve, the greater is the energy dissipation. Thus viscoelastic tissues exhibit higher damping ability [44, 45]. The depth of the embedment may significantly affect the system damping response [46]. The damping ratio is a dimensionless value used to describe damping property of a system. It is used to evaluate the viscoelastic behavior of substances [36, 47]. Damping ratio analysis provides additional information on osseointegration of dental implants [27–29] during the healing period because the trabecular bone is important for developing secondary implant stability due to its higher capacity for new bone formation and remodeling. Additionally, the trabecular bone provides a viscoelastic property at the implant/bone interface. The periodontal ligament is well known for its viscoelastic properties. It is the major damping material of teeth and acts as a shock absorber to minimize external loading [48, 49]. Nevertheless, there is no systemic research about the damping behavior of natural teeth, particularly for progressive vertical alveolar bone height loss. In our studies, as the depth of root embedded in the simulated bone decreased, the amount of bone loss increased, and the damping ratio was increased (Fig. 6). These results conformed to previous research by Todorovska [45] who reported that a system’s damping ratio is larger when the depth of the embedment is smaller.
Based on our results, damping ratio analysis is a sensitive parameter for evaluating various simulated degrees of vertical alveolar bone loss. In the rigid interface, such as tooth ankyloses (tooth to bone contact without a periodontal ligament) resonance frequency analysis shows a clearly identified boundary condition. Nonetheless, when softer tissue is present between the interfaces, like with tooth to bone contact with a periodontal ligament or implant to trabecular bone contact, the damping ratio is a more sensitive parameter for evaluating the softer tissue damping conditions. We believe that it is reasonable to suggest that damping ratio analysis is a sensitive tool in a viscoelastic surrounding, and damping ratio is a reliable measure for monitoring the status of periodontal conditions of different root types as the boundary conditions change.

**Conclusion**

These results suggested that DR is a sensitive measure of periodontal status of different root types as boundary conditions are changed. Thus, it is reasonable to suggest that DR analysis is an efficient tool to evaluate the periodontal status of teeth. DR analysis combined with RF analysis results in a more sensitive assessment of changes in the periodontal status than RF or PTV analysis alone.

### Abbreviations

PTV: periostest value; RF: resonance frequency; ANOVA: analysis of variance; DR: damping ratio; UCI: upper central incisor; UFP: upper first premolar; UFM: upper first molar.

### Authors’ contributions

KNH performed all the experiment. SYL and HMH participated in the design of the study and performed the statistical analysis. All authors read and approved the final manuscript.

### Acknowledgements

Not applicable.

### Competing interests

The authors declare that they have no competing interests.

### Availability of data and materials

Please contact author for data requests.

### Consent for publication

Not applicable.

### Ethics approval and consent to participate

Not applicable.

### Funding

Not applicable.

### Publisher’s Note

Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Received: 22 March 2017   Accepted: 26 July 2017

Published online: 03 August 2017

### References

1. Oka H, Yamamoto T, Saratani K, Kawazoe T. Application of mechanical mobility of periodontal tissues to tooth mobility examination. Med Biol Eng Comput. 1989;27:75–81.
2. Robinson PJ, Vitek RM. The relationship between gingival inflammation and resistance to probe penetration. J Periodontal Res. 1979;14:239–43.
3. Poisson AM, Caton JG, Yeaple RN, Zander HA. Histological determination of probe tip penetration into gingival sulcus of humans using an electronic pressure-sensitive probe. J Clin Periodontol. 1980;7:479–88.

4. Sykaras N, Triplet RG, Nunn ME. Effect of recombinant human bone morphogenetic protein-2 on bone regeneration and osseointegration of dental implants. Clin Oral Implants Res. 2001;12:339–49.

5. Oh JH, Chang MT. Comparison of initial implant stability measured by resonance frequency analysis between different implant systems. J Korean Acad Periodontol. 2008;38:529–34.

6. Mühlemann HR. Tooth mobility: a review of clinical aspects and research findings. J Periodontol. 1967;38:686–708.

7. Berthold C, Holst S, Schmitt J, Goellner M, Petschelt A. An evaluation of the periotest method as a tool for monitoring tooth mobility in dental traumatology. Dent Traumatol. 2010;26:120–8.

8. Andresen M, Mackie I, Worthington H. The periotest in traumatology. Part I. Does it have the properties necessary for use as a clinical device and can the measurements be interpreted? Dent Traumatol. 2003;19:214–7.

9. Campbell KM, Casas MJ, Kenny DJ, Chau T. Diagnosis of ankylosis in permanent incisors by expert ratings, periotest® and digital sound wave analysis. Dent Traumatol. 2005;21:206–12.

10. Jorge JH, Giampaolo ET, Vergani CE, Machado AL, Pavanina AC, Cardoso de Oliveira MR. Clinical evaluation of abutment teeth of removable partial denture by means of the periotest method. J Oral Rehabil. 2007;34:222–7.

11. Derhami K, Wolfart JF, Faulkner G, Grace M. Assessment of the periotest device in baseline mobility measurements of craniofacial implants. Int J Oral Maxillofac Implants. 1995;10:221–9.

12. Caulier H, Naert I, Kalk W, Jansen JA. The relationship of some histologic parameters, radiographic evaluations, and periotest measurements of oral implants: an experimental animal study. Int J Oral Maxillofac Implants. 1997;12:380–6.

13. Ioi H, Morishita T, Nakata S, Nakasima A, Nanda RS. Evaluation of physiological tooth movements within clinically normal periodontal tissues by means of periodontal pulsatlon measurements. J Periodontol. 2002;37:110–7.

14. Goellner M, Berthold C, Holst S, Wichmann M, Schmitt J. Correlations between photogrammetric measurements of tooth mobility and the periotest method. Acta Odontol Scand. 2012;70:27–35.

15. Huang HM, Lee SY, Yeh CY, Wang MS, Chang WJ, Lin CT. Natural frequency analysis of periodontal conditions in human anterior teeth. Ann Biomed Eng. 2001;29:915–20.

16. Huang HM, Yu CC, Lin CT, Chen HC, Shih YH, Lo YJ, Lee SY. Resonance frequency analysis of tooth mobility under various simulated types and degree of alveolar bony defects. Chin Dent J. 2001;10:155–64.

17. Huang HM, Lee SY, Yeh CY, Lin CT. Resonance frequency of dental implant stability with various bone quality: a numerical approach. Clin Oral Implants Res. 2002;13:65–74.

18. Huang HM, Chiu CL, Yeh CY, Lin CT, Lin LH, Lee SY. Early detection of implant healing process using resonance frequency analysis. Clin Oral Implants Res. 2003;14:437–43.

19. Kojima Y, Fukui H. Calculation of natural frequencies of teeth supported with periodontal ligament. Dent Mater J. 2007;26:254–9.

20. Yang SM, Shin SY, Kye SB. Relationship between implant stability measured by resonance frequency analysis (RFA) and bone loss during early healing period. Oral Surg Oral Med Oral Pathol Oral Radiol Endod. 2008;105:12–9.

21. Lee SY, Huang HM, Lin CY. In vivo and in vitro natural frequency analysis of periodontal conditions, an innovative method. J Periodontol. 2000;71:632–40.

22. Wang CH, Ou KL, Chang WT, Teng NC, Yu JJ, Huang HM. Detection of fracture involvement of multirooted molar using natural frequency analysis: a numerical approach. Proc Instn Mech Eng H J Eng Med. 2009;223:375–82.

23. Khan AS, Phillips MJ, Elizabeth Tanner K, Wong FS. Comparison of the visco-elastic behavior of a pre-impregnated reinforced glass fiber composite with resin-based composite. Dent Mater. 2008;24:1534–8.

24. Pantelou PD, Xirafaki AL, Panagiotopoulos E, Varakis JS, Vagenas NV, Kontoyannis CC. Modal damping for monitoring bone integrity and osteoporosis. J Biomech Eng. 2004;126:1–5.

25. Anastassopoulos G, Pantelou S, Christopoulos G. Vibrational bone characteristics versus bone density for the assessment of osteoporosis in ovariectomized rats. J Med Eng Technol. 2010;34:35–42.

26. Bhatchacharya A, Watts NB, Davis K. Dynamic bone quality: a noninvasive measure of bone’s biomechanical property in osteoporosis. J Clin Densitom. 2010;13:228–36.

27. Feng SW, Lin CT, Chang WJ, Lee SY, Cheng CH, Huang HM. Influence of simulated bone quality and cortical bone thickness on implant stability detection using resonance frequency and damping factor analysis. Int J Oral Maxillofac Implants. 2014;29:105–12.

28. Feng SW, Chang WJ, Lin CT, Lee SY, Teng NC, Huang HM. Modal damping factor detected with an impulse-forced vibration method provides additional information on osseointegration during dental implant healing. Int J Oral Maxillofac Implants. 2015;30:1333–40.

29. Feng SW, Ho KN, Chan YH, Chang KJ, Lai WY, Huang HM. Damping factor as a diagnostic parameter for assessment of osseointegration during the dental implant healing process: an experimental study in rabbits. Ann Biomed Eng. 2016;44:3668–78.

30. Benatti BB, Silverio KG, Casati MA, Sallum EA, Nocti FH. Physiological features of periodontal regeneration and approaches for periodontal tissue engineering utilizing periodontal ligament cells. J Biosci Bioeng. 2007;103:1–6.

31. Panagiotopoulos G, Kupczaik K, Cobb SN. The mechanical function of the periodontal ligament in the macaque mandible: a validation and sensitivity study using finite element analysis. J Anat. 2011;218:75–86.

32. Kobayashi M, Yamaoka H, Yamaoka M. Assessing qualitative changes in simulated periodontal ligament and alveolar bone using a non-contact electromagnetic vibration device. Clin Oral Investig. 2012;16:1161–9.

33. Hayashi M, Kobayashi C, Ogata H, Yamaoka M, Ogiso B. A nocotact vibration device for measuring implant stability. Clin Oral Implants Res. 2010;21:931–6.

34. Soares CJ, Piri ECG, Fonseca RB, Martins LRM. Influence of root embedment material and periodontal ligament simulation on fracture resistance tests. Braz Oral Res. 2005;19(1):11–6.

35. Cheng WT, Lee SY, Wu CC, Lin CT, Abiko Y, Yamamichi N, Huang HM. A newly designed resonance frequency analysis device for dental implant stability detection. Dent Mater J. 2007;26:665–71.

36. Thomson WT, Dahleh MD. Harmonically excited vibration. In: Thomson WT, Dahleh MD, editors. Theory of vibration with applications. 5th ed. Upper Saddle River, NJ: Prentice-Hall; 1998. p. 49–51.
37. Christopoulou GE, Stavropoulou A, Anastassopoulos G, Panteliou SD, Papadaki E, Karamanos NK, Panagiotopoulou E. Evaluation of modal damping factor as a diagnostic tool for osteoporosis and its relation with serum osteocalcin and collagen I N-telopeptide for monitoring the efficacy of alendronate in ovariectomized rats. J Pharm Biomed Anal. 2006;41:891–7.

38. Wang CH, Liu HW, Ou KL, Teng NC, Yu JJ, Huang HM. Natural frequency analysis of tooth stability under various simulated types and degrees of alveolar vertical bone loss. Proc Inst Mech Eng H J Biomed Eng. 2008;222:983–9.

39. Barbour ME, Parker DM, Jandt KD. Enamel dissolution as a function of solution degree of saturation with respect to hydroxyapatite: a nanoindentation study. J Collid Interface Sci. 2003;265:9–14.

40. Machado C, Lacefield W, Catledge A. Human enamel nanohardness, elastic modulus and surface integrity after beverage contact. Braz Dent J. 2008;19:68–72.

41. Shen LK, Huang HM, Yu JJ, Lee SY, Lee CM, Hsieh SC. Effects of periodontal bone loss on the natural frequency of human canine: a three-dimensional finite element analysis. J Dent Sci. 2009;4:81–6.

42. Schultz W, D’hoedt B, Lukas D, Mühlenbradt L, Scholz F, Bretsch J, Frey D, Guzat H, König M, Markl M, Quante F, Schief A, Topkaya A. Periotest—a new measurement process for periodontal function. Zahnarzt. 1983;73:1229–40.

43. Doshi Y, Mani A, Marawar PP, Mishra P. A clinical study on mobility of teeth as assessed through their damping characteristics and progress of periodontal disease using advanced diagnostic aids: mobilometer and florida probe. J Int Clin Dent Res Organ. 2010;2:12–9.

44. Chen JT, You DW. Hysteretic damping revisited. Adv Eng Softw. 1997;28:165–71.

45. Adsanizadeh S, Li LP. Visco-hyperelastic constitutive modeling of soft tissues based on short and long-term internal variables. Biomed Eng Online. 2015;14:29.

46. Todorovska MI. Effects of the depth of the embedment on the system response during building-soil interaction. Soil Dyn Earthq Eng. 1992;11:111–23.

47. Abdel-Wahab AA, Alam K, Silberschmidt VW. Analysis of anisotropic viscoelastoplastic properties of cortical bone tissues. J Mech Behav Biomed Mater. 2011;4:807–20.

48. Mei ML, Chen YM, Li H, Chu CH. Influence of the indirect restoration design on the fracture resistance: a finite element study. Biomed Eng Online. 2016;15:3.

49. Huang SF, Chen WR, Lin CL. Biomechanical interactions of endodontically treated tooth implant-supported prosthesis under fatigue test with acoustic emission monitoring. Biomed Eng Online. 2016;15:23.