Photonic molecules with a tunable inter-cavity gap

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Optical micro-resonators have broad applications. They are used, for example, to enhance light–matter interactions in optical sensors or as model systems for investigating fundamental physical mechanisms in cavity quantum electrodynamics. Coupling two or more micro-cavities is particularly interesting as it enhances the design freedom and the field of application. In this context, achieving tunability of the coupling strength and hence the inter-cavity gap is of utmost importance for adjusting the properties of the coupled micro-resonator system. In this paper, we report on a novel coupling approach that allows highly precise tuning of the coupling gap of polymeric micro-resonators that are fabricated side by side on a common substrate. We structure goblet-shaped whispering-gallery-mode resonators on an elastic silicone-based polymer substrate by direct laser writing. The silicone substrate is mechanically stretched in order to exploit the lateral shrinkage to reduce the coupling gap. Incorporating a laser dye into the micro-resonators transforms the cavities into micro-lasers that can be pumped optically. We have investigated the lasing emission by micro-photoluminescence spectroscopy, focusing on the spatial localization of the modes. Our results demonstrate the formation of photonic molecules consisting of two or even three resonators, for which the coupling strengths and hence the lasing performance can be precisely tuned. Flexibility and tunability are key elements in future photonics, making our approach interesting for various photonic applications. For instance, as our coupling approach can also be extended to larger cavity arrays, it might serve as a platform for tunable coupled-resonator optical waveguide devices.

Keywords: coupled resonators; photonic molecules; micro-lasers; tunable coupling gap; whispering gallery mode resonators

INTRODUCTION

Whispering-gallery-mode (WGM) resonators have emerged as versatile photonic structures for fundamental investigations in quantum optics1–9, as well as for applications in optical sensing6–9, laser emission10–12 and telecommunication technology13–15. Among the various types of micro-cavities16–17, WGM resonators are most ideally suited for optical coupling to form so-called photonic molecules (PMs). In PMs, optical modes interact to create super-modes extending over the entire ensemble of coupled cavities18,19. This capability further enhances the performance of WGM resonators and broadens the scope of their applications. In lasing devices, coupling to PMs enables mode selection and single-mode emission20–22 owing to the Vernier effect, which also enhances the sensitivity of cascaded WGM micro-ring resonators23,24. Coupled dye-doped polymer micro-fibers can be used as enhanced refractive index sensors25. Furthermore, the angular emission profile of PMs can be tailored—even to be uni-directional26,25. Coupled resonators also show an enhanced Q factor27,28. They are used as optical filters and switches, where line-shape and bandwidth tuning lead to improved optical filtering responses29–31. In addition, the increased electromagnetic field in the coupling gap associated with the super-modes results in an enhanced sensitivity for PM sensors20,32.

The up-scaling of photonic molecules to arrays of coupled resonators leads to so-called coupled-resonator optical waveguides (CROWs). CROWs have unique dispersion properties allowing their usage as compact delay lines33–35. The group velocity of light propagating in a CROW is dependent on the coupling coefficient κ, which describes the coupling strength between the individual micro-cavities36,37. Realizing adjustable gap widths and coupling coefficients would hence pave the way to tunable and switchable CROW devices.

Thus far, flexible coupling between waveguides and optical micro-resonators has been established, for example, by the use of micro-electrical mechanical systems38,39. Tunable photonic crystals have also been achieved by micro-electrical mechanical system approaches40,41. However, direct dynamical coupling among adjacent resonators has not been achieved in a viable way. The micro-cavities are typically structured on rigid substrates by lithography and are therefore intrinsically inflexible after fabrication20,25,42, excluding dynamic tunability in general. Sometimes, additional surface modification after fabrication is required to reduce the gap width to the order of the...
wavelength, which is essential for optical coupling. The tuning of coupling gaps can be achieved when individual cavities are fixed to nano-positioning systems. However, this approach is experimentally challenging, as precise alignment is essential and vulnerable to mechanical vibrations. It is further limited to PMs consisting of only two micro-resonators and is not scalable to CROWs.

In this article, we present a novel coupling approach for the flexible formation of PMs from WGM micro-resonators. This approach is based on resonator fabrication by direct laser writing (DLW) on elastomer substrates. It enables the controllable and reversible tunability of the inter-cavity gap separation for resonators co-integrated side by side on the same substrate. We demonstrate the occurrence of super-modes not only for a pair of resonators but also for a linear array of three.

MATERIALS AND METHODS
Fabrication of polymeric micro-lasers on elastomer substrates

We have fabricated on-chip yet flexible polymeric photonic molecules consisting of dye-doped WGM resonators on an elastic polymer substrate. These high-Q resonators have been structured next to each other on the substrate, as shown in Figure 1a–1d. For the substrate, we used commercially available polydimethylsiloxane (PDMS, SYLGARD 184 Silicone Elastomer, Dow Corning GmbH, Wiesbaden, Germany). The weight ratio of the elastomer and curing agent was chosen to be 13:1 rather than the commonly used 10:1 ratio in order to enhance the substrate elasticity. PDMS was then poured into a casting mold on a glass slide, which was previously rinsed thoroughly with acetone and isopropanol to obtain a clean and flat surface for the subsequent processes, as shown in Figure 1a. Next, PDMS was cured at room temperature for at least 48 h. Afterwards, the ∼2 mm-thick PDMS layer was pulled off the glass slide and used as a substrate, providing a smooth surface for the micro-resonators. In order to promote adhesion of the resonators, the PDMS surface was activated using O2 plasma etching, as illustrated in Figure 1c. After exposure, the unpolymerized photoresist was then developed using a solution of methyl isobutyl ketone and isopropanol for 12 min. After subsequent rinsing with acetone and isopropanol and drying in a nitrogen atmosphere, the polymerized resonators remain on the PDMS substrate, as shown in Figure 1d.

Using this fabrication procedure, arrays of closely spaced micro-resonators can be structured in arbitrary arrangements. The achievable inter-cavity gaps between adjacent polymer resonators are typically near 1 μm. This value is actually larger than the minimum gap size achieved with electron beam lithography of polymeric WGM cavities (on the order of 300 nm). However, even this narrow gap size must be further reduced post fabrication to below 200 nm for the successful optical coupling of resonators. The advantage of DLW, however, is that non-conductive substrates (for example, elastomers) can be used, facilitating tunable coupling.

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Figure 1 Illustration of the process steps to fabricate polymer WGM micro-lasers on PDMS. A PDMS substrate with a flat surface is fabricated by pouring silicone mixed with curing agent into a mold on a glass slide (a). To enhance adhesion, the PDMS surface is activated using O2 plasma etching and silanization (b). Polymer micro-resonators are structured in sandwich-type geometry by DLW (c). The unpolymerized resist is removed by chemical development, yielding micro-lasers on a flexible substrate (d).
Mechanical tuning of the coupling gap
To tune the coupling gap, the flexible, non-auxetic PDMS substrate is fixed between two clamps and stretched using a micrometer screw. By orienting the major axis of the PM perpendicular to the stretching direction, the lateral contraction of the elastomer substrate can be exploited in order to decrease the inter-cavity gaps. This coupling mechanism is illustrated in Figure 2a, with scanning electron micrographs of two and three adjacent goblet-shaped micro-cavities shown in Figure 2b and 2c.

In order to control the coupling gap, the lateral substrate shrinkage has been calibrated. For this purpose, a grid was drawn onto an identical PDMS substrate, and different stretching forces were applied on the substrate. The lateral substrate shrinkage with respect to the substrate expansion was determined from photographic images. A linear relation between the substrate expansion and the coupling gap was found. More information about the substrate calibration can be found in the Supplementary Information.

Spatially resolved spectroscopy of (super-) modes
Optical characterization of the PM lasers was performed by microphotoluminescence (μ-PL) spectroscopy. The micro-lasers were pumped with 10 ns pulses of a frequency-doubled neodymium-doped yttrium orthovanadate (Nd:YVO4) laser at a wavelength of 532 nm and a repetition rate of 20 Hz. Pulsed excitation with pump pulses shorter than the typical intersystem crossing rate of the dyes, $k_{IC} \sim 100 \text{ ns}^{49}$, is required for investigating lasing in micro-cavities because it can prevent fluorescence quenching of the dyes owing to triplet formation$^{50}$. The pump beam is focused at an incident angle of $\sim 45^\circ$ to a spot size of $\sim 100 \mu\text{m}$, which allows the homogenous illumination of all cavities involved in the coupling process. The resonators can simultaneously be imaged on a camera and on the entrance slit of a spectrometer using optics that include a long-working distance microscope objective (magnification of $50 \times$ and numerical aperture of 0.4). In this way, the PL emission can be analyzed in a spectrometer (focal length = 0.5 m, 1200 or 2400 lines mm$^{-1}$ grating) equipped with a charge-coupled device camera. Illustration schemes of the setup can be found in earlier publications$^{20,51}$. By orienting the sample so that the major axis of the PM is aligned parallel to the entrance slit (Figure 3), the μ-PL setup allows the emitted light from the resonators to be not only spectrally resolved but also spatially resolved: WGM lasing emission from the distant rims of the cavities as well as from the coupling region can be simultaneously recorded and can enable the distinction of non-coupled lasing modes of the individual cavities and lasing super-modes of the coupled photonic molecule.

RESULTS AND DISCUSSION
To investigate the coupling effects among polymer micro-resonators, two different experiments were performed. First, the results of the tunable coupling of two size-mismatched micro-lasers are presented; then, we show the formation of even larger PMs consisting of a linear chain of three equally sized micro-cavities.

Flexible formation of photonic molecules consisting of two micro-lasers
To demonstrate the flexible formation of PMs, goblet-shaped micro-resonators with diameters of 30 and 50 $\mu\text{m}$ were structured on a PDMS substrate with an inter-cavity gap of 3 $\mu\text{m}$. The cavities were pumped with an energy density of 960 $\mu\text{J pulse}^{-1} \text{cm}^{-2}$. The lasing thresholds for single resonators of these types were measured to be as low as 230 (resonators with 50 $\mu\text{m}$ diameter) and 430 $\mu\text{J pulse}^{-1} \text{cm}^{-2}$ (resonators with 30 $\mu\text{m}$ diameter). Hence, in our experiment, the

![Figure 2](image-url)

Figure 2 (a) Schematic of the tunable coupling mechanism by stretching a PDMS substrate (blue arrows) and exploiting the lateral shrinkage (green arrows). The dotted lines show the pre-stretching state of the substrate and the inter-cavity distance, whereas the solid line represents the substrate after applying a force in the $x$ direction. The red circles illustrate the resonators with a reduced gap after expansion. (b) Scanning electron micrograph of two goblet-shaped polymeric micro-resonators fabricated by DLW on a PDMS elastomer substrate with diameters of 30 and 50 $\mu\text{m}$, and a designed inter-cavity gap of 3 $\mu\text{m}$. (c) Scanning electron micrograph of three equal-sized polymeric micro-goblets with diameters of 30 $\mu\text{m}$.
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Figure 3 Spatially resolved µ-PL spectra of micro-lasers with diameters of 30 and 50 µm indicating the localization of WGM lasing modes for the uncoupled case (Case A) and the coupled case (Case B). Whereas in Case A, the cavities are considered to be independent micro-lasers with modes in either cavity, Case B shows the coupled system with lasing super-modes extending over both resonators.

resonators are pumped well above the typical lasing threshold energy density. In order to determine the quality factors of the cavities, transmission measurements through a tapered glass fiber approaching the resonators were performed, yielding Q factors up to $7.9 \times 10^{4}$ (50 µm diameter) and $2.3 \times 10^{4}$ (30 µm diameter). With this method, we also confirmed the free spectral ranges expected based on theory ($\text{FSR}_{50 \mu m} = 1.69 \text{ nm}$, $\text{FSR}_{30 \mu m} = 2.77 \text{ nm}$). For more details on the characteristics of the resonators, see the Supplementary Information.

Two of the recorded spatially resolved µ-PL spectra are shown in Figure 3. Case A represents the spectrum taken at the designed initial gap distance of 3 µm. High intensities of the WGM lasing emission can clearly be localized at the rim region of the cavities. The background fluorescence in the middle region originates from the pedestal, which is also dye-doped. The modes are clearly localized either in the upper or in the lower cavity, and both resonators can thus be considered as independent micro-lasers.

Uncoupled lasing modes have similar intensities at the rims of one cavity but no or significantly less intensity in the other cavity. This situation is illustrated for the mode at 607.46 nm, framed with a white rectangle and marked with a blue square in Case A. The small residual intensity at the lower rim of the lower resonator can be explained through scattering of the radiated laser emission from the upper resonator at this rim region. Clearly, the intensities in the upper and lower resonator are substantially different, showing that the mode is solely resonant in the upper cavity. To underline this point, the cavities were also pumped individually before the coupling experiment. In that case also, no lasing mode was observed in the lower resonator at this spectral position, proving that the residual intensity in the lower cavity is not due to a resonant mode but rather to the explained scattering. Consequently, the initial gap is still too large for photon exchange among the cavities.

Reducing the coupling gap by the above method actually leads to a photon exchange among the cavities and the formation of a PM. The experimental results nicely illustrate the interplay of the modal optical gain and the Vernier effect. Single active WGM resonators typically show a rich spectrum of lasing modes where, in addition to the fundamental modes, a multitude of higher-order modes compete for the optical gain. Moving a second WGM resonator into the evanescent field of the lasing modes leads to optical losses unless a resonance of the second cavity is found at the same wavelength. The former scenario leads to an increasing lasing threshold or even quenching of the lasing, while the latter results in the formation of extended super-modes (Vernier effect). Of course, the coupling strength and overlap of the modal field with the gain region determine the threshold and intensity of the lasing super-modes. Overall, a reduction of lasing modes is observed starting at the threshold and resulting in single-mode lasing for small gaps.

Flexible gap tuning and its influence on the modal structure
In the following, we intend to focus on the flexible tuning of the inter-cavity gap and its impact on the modal structure in the PM. The experimental results nicely illustrate the interplay of the modal optical gain and the Vernier effect. Single active WGM resonators typically show a rich spectrum of lasing modes where, in addition to the fundamental modes, a multitude of higher-order modes compete for the optical gain. Moving a second WGM resonator into the evanescent field of the lasing modes leads to optical losses unless a resonance of the second cavity is found at the same wavelength. The former scenario leads to an increasing lasing threshold or even quenching of the lasing, while the latter results in the formation of extended super-modes (Vernier effect). Of course, the coupling strength and overlap of the modal field with the gain region determine the threshold and intensity of the lasing super-modes. Overall, a reduction of lasing modes is observed starting at the threshold and resulting in single-mode lasing for small gaps.

However, we show below that new lasing super-modes also emerge that have not been observed above the threshold in uncoupled resonators.

The scenarios discussed above are illustrated in Figure 3: (i) a super-mode occurs where in the uncoupled arrangement a lasing mode was observed only in one of the cavities (example marked by red triangle); (ii) a lasing super-mode arises at a wavelength where no lasing modes were previously observed (example marked by a black circle); and (iii) the attenuation of an individual cavity mode leads to its extinction (example marked by a blue square). More details on the dependence of the modal structure on the coupling gap are reflected in Figure 4a and 4b. Here we plot the integrated intensities (now on a clearer linear
rather than logarithmic scale) of those example modes, illustrating scenarios (i)–(iii) as a function of gap size between the two resonators. To interpret the results, one must consider that a minor part of the observed intensity can be due to light scattering from the neighboring resonator. This fact and how to avoid misinterpretation are discussed above. Furthermore, as the measured intensity is mainly due to laser light scattered from surface imperfections toward the detector (perfect high-Q WGM resonators would not show bright emission), we cannot detect absolute intensity values but rather only trends of their evolution. Nevertheless, the pronounced trends of the lasing intensities in Figure 4 in combination with the above identified localization of the modes (Figure 3) convincingly demonstrate the tunable optical coupling of the two cavities.

Specifically, to record the spectra shown in Figure 4, we used the same cavity pair and experimental conditions used in Figure 3. The spectra are vertically binned over the full extent of the spectrometer slit and plotted for inter-cavity gaps smaller than 300 nm. The change in the photoluminescence intensity is tracked as a function of the coupling gap, which can be tuned with a precision of 12 nm (Supplementary Information). After each mechanical tuning step, the detection path is realigned for maximum signal.

The mode at 613.34 nm (red triangles) shows a steep increase with decreasing coupling gap and reflects scenario (i) described above. Here the lasing mode was already visible in one of the cavities before coupling. The mode at 610.38 nm (black circles) shows a similar rise but has no precursors in the single cavities (scenario (ii)). The super-mode has access to a larger gain volume, boosting it beyond the threshold. The mode located at 607.46 nm (blue squares) shows a decrease in intensity until complete extinction owing to the increased loss when no matching mode is present in the second cavity (scenario (iii)). By increasing the coupling gap through releasing the substrate strain back to the initial substrate state, the photoluminescence spectrum changes back to the uncoupled case with the same individual lasing modes as before in the individual resonators. This behavior illustrates the reversibility of the applied coupling scheme using elastomer substrates.

The intensity trends documented in Figures 3 and 4 are exponential within experimental uncertainties. To illustrate this point, exponential trend lines (no fits) have been added to the intensity increase of the arising super-modes. The slightly different onset of the two super-modes can be attributed to differences in the overlaps of the electromagnetic fields and therefore different coupling strengths. This behavior is analogous to the reduction of the number of modes with decreasing coupling gap investigated by Grossmann et al. Here the modes with different field overlaps also vanish for different gap widths. The observed exponential increase in intensity can be attributed to the exponential dependence of the inter-cavity photon tunneling rate on the gap size.

In order to understand these experimental findings in more detail, we compared them with theoretical expectations. An analytic expression for the coupling strength between two micro-resonators was derived by Little et al. They introduced the coupling parameter κ, the fraction of the amplitude of the electric field coupled from one resonator to the other. Accordingly, κ² is also called the “power coupling coefficient.” The coupling parameter κ was shown to increase exponentially with a decreasing coupling gap width g. On the basis of this theoretical model, we calculated the coupling parameter κ(g) for the investigated size-mismatched PM (see Supplementary Information for details). Coupling parameters begin to become sizable for gap separations below 300 nm, with an exponential increase for decreasing gaps. This result is in good accordance with the intensity trends shown in Figure 4. For the vanishing individual modes, the coupling losses reflected by the decreasing lasing intensity increase significantly for gaps smaller than 300 nm (κ(300 nm) = 0.007). For coupling gap sizes near 150 nm (κ(150 nm) = 0.04), losses finally lead to extinction of the mode. In contrast, for matching resonances in both cavities, obviously no losses are introduced. Photon exchange and build-up of the super-modes, however, can only occur for coupling coefficients κ well above zero. Thus, for the same magnitude of coupling as above (κ(150 nm)), the super-mode intensity begins to increase in agreement with the experimental observation.

Flexible formation of photonic molecules consisting of three micro-lasers

Thus far, we have concentrated on the formation of a PM consisting of two micro-lasers and the tunability of its coupling gap. Now, we will demonstrate that the approach using elastomer substrates can be...
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extended to larger cavity arrays. We give below an example of a flexible, on-chip PM consisting of three micro-cavities.

A linear array of three goblet-shaped WGM micro-lasers with equal diameters of 30 μm has been fabricated as described above. The cavities are pumped above their lasing threshold with a pump energy density of 1130 μJ pulse⁻¹ cm⁻² similar to the conditions above. Again, spatially resolved μ-PL measurements allow a clear distinction between the uncoupled (Case A) and the coupled case (Case B), as shown in Figure 5. In Case A, again, only modes localized in the individual cavities can be observed. In Case B, the overall spectrum has changed markedly. Reducing the gap from a designed initial gap distance of 2 μm to ~ 55 nm allows photon exchange among the single micro-lasers. Thus, delocalized super-modes that extend over all resonators involved can be clearly detected, demonstrating the successful optical coupling of the three cavities. On the other hand, many individual lasing modes present in Case A (see, for example, the low-energy part of spectrum) have vanished in Case B, as expected owing to increased optical coupling losses related to the Vernier effect. After releasing the substrate, the coupled-case spectrum reverts to the initial PL spectrum, with the same individual modes as before straining the substrate.

These data prove that our fabrication scheme enables the flexible formation of PMs consisting of three resonators arranged in a linear chain on a polymer chip. As the coupling mechanism and the fabrication are not limited to three micro-resonators, it should be possible to apply this approach to couple an even larger number of cavities.

CONCLUSIONS

To summarize, we have presented an approach that allows the post-fabrication flexible tuning of the coupling gap width between two or three optical micro-resonators. Goblet-shaped polymer WGM micro-lasers were structured in a linear arrangement on an elastomer substrate by DLW. Then, the substrate was mechanically stretched in order to exploit a lateral substrate contraction perpendicular to the stretching direction. This method allows fine-tuning of the coupling gap with a precision comparable to a nano-positioning piezo system but with the significant advantage that the cavities are arranged on one polymer chip. Coupling of the resonators to photonic molecules was demonstrated by the observation of super-mode lasing in spatially resolved μ-PL spectroscopy. Super-modes (non-super-modes) show a distinct increase (vanishing) of lasing intensity, which can be attributed to the exponential increase of the coupling strength and the inter-cavity tunneling rate.

The presented coupling approach can in principle be further extended to realize even larger coupled on-chip cavity arrays. In this way, our approach, together with tapered fiber coupling or 3D polymer waveguide structuring⁵⁶, could enable the fabrication of tunable CROW devices. Of course, the focus of the work presented here is not the technical improvement of existing CROWs. However, we demonstrated that new and important degrees of freedom such as flexibility and tunability can be added. There is the prospect that novel features associated not only with CROWs but also with other photonic structures arise owing to this tunability evoked by the use of elastomer substrates. Both fundamental aspects such modal splitting or slow light propagation and applications such as tunable filters or switches can be addressed in a more elaborate way.

CONFLICT OF INTEREST

The authors declare no conflict of interest.

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