ON THE RARITY OF X-RAY BINARIES WITH NAKED HELIUM DONORS

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ABSTRACT

The paucity of known high-mass X-ray binaries (HMXBs) with naked He donor stars (hereafter He star) in the Galaxy has been noted over the years as a surprising fact, given the significant number of Galactic HMXBs containing H-rich donors, which are expected to be their progenitors. This contrast has further sharpened in light of recent observations uncovering a preponderance of HMXBs hosting loosely bound Be donors orbiting neutron stars (NSs), which would be expected to naturally evolve into He-HMXBs through dynamical mass transfer onto the NS and a common-envelope (CE) phase. Hence, reconciling the large population of Be-HMXBs with the observation of only one He-HMXB can help constrain the dynamics of CE physics. Here, we use detailed stellar structure and evolution models and show that binary mergers of HMXBs during CE events must be common in order to resolve the tension between these observed populations. We find that, quantitatively, this scenario remains consistent with the typically adopted energy parameterization of CE evolution, yielding expected populations which are not at odds with current observations. However, future observations which better constrain the underlying population of loosely bound O/B–NS binaries are likely to place significant constraints on the efficiency of CE ejection.

Key words: galaxies: starburst – stars: emission-line, Be – stars: Wolf–Rayet – X-rays: binaries

Online-only material: color figures

1. INTRODUCTION

As a star in a binary system evolves off of the main sequence (MS) and radially expands, it can overflow its Roche lobe and begin transferring mass onto its companion. If this transfer proceeds on a timescale shorter than the timescale in which the accretor can achieve thermal equilibrium, a common envelope (CE) develops and the stars begin to orbit through a combined atmosphere. Energy is then transferred from the binary orbit to the CE through frictional forces and torques which unbind the CE gases (Iben & Livio 1993; Taam & Sandquist 2000). This process has long been discussed as the dominant mechanism for forming tight binaries from widely separated systems hosting one or two massive stars; it is thought to produce many closely interacting binaries such as Cataclysmic Variables (Paczynski 1976) and X-ray Binaries (Eggleton & Verbunt 1986; Bailyn & Grindlay 1987).

Unfortunately the hydrodynamics and long-term evolution during the CE phase are not well understood, making it difficult to accurately determine the efficiency of energy transfer from the binary orbit into the ejection of the CE. While advancements in computational hydrodynamics have elucidated several trends near the onset of the CE phase (Rasio & Livio 1996; Sandquist et al. 2000; Taam & Ricker 2006; Ricker & Taam 2008), a simple parameterization must be employed in situations where a population of binaries is to be considered. To this end, Webbink (1984) incorporated the myriad uncertainties of CE evolution into a single parameter ΛCE, which governs the efficiency of transferring gravitational energy into the complete removal of the CE. Within this framework, a relation between the initial and final orbital separations can be written as

\[
\alpha_{\text{CE}} \left[ \frac{G M_e M_a}{a_f} - \frac{G (M_e + M_*) M_a}{a_i} \right] = |E_{\text{bind}}|, \tag{1}
\]

where \( G \) is the gravitational constant, \( a_i \) and \( a_f \) are the initial and final orbital separations, \( M_* \), \( M_e \), and \( M_a \) are the masses of the donor core, donor envelope, and accretor, respectively, and \( E_{\text{bind}} \) is the energy necessary to unbind the CE. The value of \( E_{\text{bind}} \) includes not only the (negative) gravitational binding energy, but also terms relating to the (positive) thermal energy of the plasma gas, the ionization of H and He, and the disassociation of \( \text{H}_2 \) (Han et al. 1994, 1995).

Another uncertainty entering the calculation of \( E_{\text{bind}} \) is the definition of the core-envelope boundaries (Dewi & Tauris 2000; Loveridge et al. 2011). As a rough definition of the stellar core, we assume the boundary to occur at the radius where the mass fraction of H drops below a critical value \( X_{\text{min}} \). Here, we set \( X_{\text{min}} = 0.1 \) and investigate the effect of changing this parameter in what follows.

One long-standing expectation from models of binary evolution concerns the resilient population of high-mass X-ray binaries (HMXBs) consisting of neutron stars (NSs) accreting matter from the wind of naked He donors (He-HMXB). Such binaries are expected to form when the observed population of O/B-HMXBs evolves through a CE phase of the supergiant stellar component. The lack of observed He-HMXBs is particularly puzzling in light of recent observations uncovering an unexpectedly large population of HMXBs with Be-type stars (B-type stars which show emission-line (Be) spectra). Since each Be-HMXB contains an NS accretor along with a massive (O8–B2) donor in a wide orbital period \( (P_{\text{orb}} > 30 \text{ days}) \), these systems are the expected progenitors of a bright HMXB population with He donors. Specifically, as both the orbital separation of observed Be-HMXBs is smaller than the star’s supergiant radius and the mass ratio between the Be donor and NS is large, Be-HMXBs inevitably evolve into a CE. If the binary survives the CE event, the resultant system would contain an He star coupled with an NS in a relatively tight orbit. Since He
stars can experience significant mass loss due to stellar winds (de Jager et al. 1988), we would naively expect to observe such binaries as bright He-HMXBs. At least 81 galactic Be-HMXBs are currently observed, with 69 reported by both Raguzova & Popov (2005) and Belczynski & Ziolkowski (2009), and numerous references therein. The donor mass, orbital period, and eccentricity are denoted by $M_{\text{don}}, P_{\text{orb}},$ and $e$, respectively. Each donor mass is derived from the spectral classification using Table VIII of Habets & Heintze (1981).

In the present analysis, we use detailed stellar structure and evolution models to investigate whether the discrepancy between Be-HMXB and He-HMXB observations can be used to place constraints on the dynamics of the CE event and specifically on $\alpha_{\text{CE}}$. In Section 2, we describe the modeling codes developed to calculate the orbital parameters of XRBs immediately before and after the CE. In Section 3, we use the currently observed sample of Be-HMXBs with measured orbital periods and eccentricities, and find that detailed calculations of massive-star binding energies and the typically adopted energy parameterization of CE evolution are consistent with the observed Galactic sample of one He-HMXB. In Section 4, we investigate whether further limits can be placed on $\alpha_{\text{CE}}$ by simulating a grid of widely separated O/B–NS binaries and determining the survival probability of He-HMXB systems as a function of $\alpha_{\text{CE}}$. In this way, we address the question of how a significant population of undiscovered O/B–NS binaries with wide orbits could further constrain energy deposition during the CE phase. We conclude in Section 5 with a discussion of how future observations could be used to place further constraints on $\alpha_{\text{CE}}$.

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**Table 1**

| Name          | Spectroscopy | $M_{\text{don}}$ ($M_\odot$) | $P_{\text{orb}}$ (days) | $e$  |
|---------------|--------------|-------------------------------|--------------------------|------|
| γ-Cas         | B0.5 Ve      | 13.8                          | 203.59                   | 0.26 |
| 0115+634      | B0.2 Ve      | 14.9                          | 24.3                     | 0.34 |
| 0236+610      | B0.5 Ve      | 13.8                          | 26.5                     | 0.55 |
| 0331+430      | OS-9 Ve      | 23.0                          | 34.3                     | 0.3  |
| 0352+309      | O9.5 IIe-B0 Ve | 16.7                         | 250                      | 0.11 |
| 0535+262      | B0 IIIe      | 15.6                          | 111                      | 0.47 |
| 0834+430      | B0-2 III-Ve  | 12.0                          | 105.8                    | 0.12 |
| J1008-57      | O9e-B1e      | 15.6                          | 247.5                    | 0.66 |
| 1417-624      | B1 Ve        | 12.0                          | 42.1                     | 0.446|
| J1946+274     | B0-1 IV-Ve   | 13.8                          | 169.2                    | 0.33 |
| J1948+32      | B0 Ve        | 15.6                          | 40.2                     | 0.03 |
| 2030+375      | B0e          | 15.6                          | 46.03                    | 0.4  |
| J2103.5+4545  | B0 Ve        | 15.6                          | 12.67                    | 0.40 |

Notes. Data obtained from Raguzova & Popov (2005) and Belczynski & Ziolkowski (2009), and numerous references therein. The donor mass inferred spectroscopically (De Donder et al. 1997; Lommen et al. 2005). The mis-match between the various definitions is further complicated by the fact that a low-mass He star ($M_{\text{don}} < 1.5 M_\odot$) undergoing Roche-lobe overflow during the period of RLO, while systems with He-core burning during RLO instead become white dwarf–NS binaries. However, they do not discuss the X-ray characteristics of their He-HMXB population.

Additionally, a significant effect has focused also on the population of observed runaway WRs, which may be host compact object partners. Moffat et al. (1982a, 1982b) present spectroscopic observations of such systems, but did not detect any X-ray bright source. Population synthesis studies targeting He stars more massive than $7 M_\odot$ found that only a small portion (1%–2%) of the observed runaway binaries hosting an O-star and an He star may eventually evolve into He-HMXBs. Subsequent work by Vanbeveren et al. (1998a) found that at most 3% of the galactic population of massive He stars should be found in binaries containing a compact object. Both studies determined the paucity of observed He-HMXBs to be primarily due to the effect of disruptions due to the natal kick imparted to the compact objects at formation, as well as the probability of mergers during CE events. However, these results cannot be directly applied to our study of He-HXMBs stemming from the observed Be-HMXB population, as we know that the system must survive as an intact binary through the NS natal kick. In any case, such population of runaway He stars is unlikely the evolutionary outcome of a population like the observed Be-HMXBs as the high spatial velocities of these systems are likely associated with the formation of the compact object and the observed O/B-HMXBs show significantly smaller spatial velocities (Chevalier & Ilovaisky 1998; van den Heuvel et al. 2000).

In the present analysis, we use detailed stellar structure and evolution models to investigate whether the discrepancy between Be-HMXB and He-HMXB observations can be used to place constraints on the dynamics of the CE event and specifically on $\alpha_{\text{CE}}$. In Section 2, we describe the modeling codes developed to calculate the orbital parameters of XRBs immediately before and after the CE. In Section 3, we use the currently observed sample of Be-HMXBs with measured orbital periods and eccentricities, and find that detailed calculations of massive-star binding energies and the typically adopted energy parameterization of CE evolution are consistent with the observed Galactic sample of one He-HMXB. In Section 4, we investigate whether further limits can be placed on $\alpha_{\text{CE}}$ by simulating a grid of widely separated O/B–NS binaries and determining the survival probability of He-HMXB systems as a function of $\alpha_{\text{CE}}$. In this way, we address the question of how a significant population of undiscovered O/B–NS binaries with wide orbits could further constrain energy deposition during the CE phase. We conclude in Section 5 with a discussion of how future observations could be used to place further constraints on $\alpha_{\text{CE}}$. 

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We have developed a detailed orbital evolution code suitable for investigating XRBs. This code tracks the evolution in time of the orbital separation and eccentricity of the binary, and the spin of the stellar component, accounting for the competing effects of stellar wind mass loss, wind accretion, tides exerted from the compact object onto the star, and angular momentum loss via gravitational radiation. To account for changes in the stellar properties due to natural stellar evolution, the orbital evolution code is coupled to a detailed stellar structure and evolution code. The stellar evolution models are calculated with an up-to-date version of the stellar evolution code STARS (Eggleton 1971, 1973; Eggleton & Kiseleva-Eggleton 2002; Pols et al. 1995), while the NS is considered as a 1.4 $M_\odot$ point mass. With this code, we follow the orbital evolution of Be-XRBs from the formation of the NS to the onset of RLO, which corresponds to the beginning of the CE phase. At this stage we extract from the stellar model the donor’s parameters (e.g., core and envelope masses, envelope binding energy, and spin) as well as the computed orbital separation and eccentricity.

Tidal evolution is calculated in the standard weak-friction approximation (Zahn 1977, 1989), following the formalism of Hut (1981). Specifically, we integrate numerically the set of differential equations as presented in Section 3.3 of Belczynski et al. (2008), with the only modification being in the second-order tidal coefficient $E_2$. For this coefficient, we adopt a stellar model from Claret (2004) with a mass of $\sim 16 M_\odot$ at solar metallicity and derive $E_2$ as

$$\log E_2 = -5.71 - 2.51 \cdot \tau_{\text{MS}}^{17284.8} - 0.69 \cdot \tau_{\text{MS}}^{74.24} - 2.30 \cdot \tau_{\text{MS}}^{10},$$

where $\tau_{\text{MS}}$ is time in units of the MS lifetime. The fitting formula has only a very weak dependence on the initial mass in the observed range for the Be donor mass. The evolution of the orbital separation and eccentricity driven by stellar wind are calculated following Hurley et al. (2002). If the primary loses mass $\Delta M_1$, the orbit loses $\Delta M_1 R_1^3 \Omega_{\text{orb}}$ of angular momentum. If the secondary accretes some of this mass $\Delta M_2$, then $\Delta M_2 R_2^3 \Omega_{\text{orb}}$ is returned to the orbit, where $\Omega_{\text{orb}}$ is the orbital frequency and $R_1$ is the radius of the primary. The time evolution of the rotational frequency driven by stellar wind follows Hurley et al. (2000) and we assume that all the mass is lost uniformly at the surface of the star. The evolution of the orbital separation and eccentricity due to gravitational radiation is calculated following Junker & Schaefer (1992). The accretion efficiency is calculated according to Bondi & Hoyle (1944) following Section 4.2 of Belczynski et al. (2008).

For each time step during the orbital evolution, we compute the Roche-lobe radius of the star at periastron (Sepinsky et al. 2007) and halt the calculation at the onset of the CE phase. At this stage we extract the relevant binary and stellar parameters (see Equation (1)) and calculate the resultant orbital parameters of the binary system from the energy prescription for CE evolution. If the radius of the donor star is found to exceed its Roche lobe after the application of the CE prescriptions, we consider the system to end in a binary merger.

Here, we note that the mass-loss rate associated with the wind of an He star is uncertain and this, in turns, affects the X-ray detectability of any surviving He–NS binary. Two very different models are quoted in the literature. First, following the models of Hurley et al. (2000) we assign a single power law to the mass loss spectrum for all He stars stemming from massive binaries given by

$$\dot{M}_{\text{He}} = 1 \times 10^{-13} (L/L_\odot)^{1.5}.$$  (3)

However, work by Nugis & Lamers (2000) and Nelemans & van den Heuvel (2001) have produced a broken power law where the mass loss declines precipitously for lower-mass He stars. The best fit given by Dewi et al. (2002, Equation (6)) follows

$$\dot{M}_{\text{He}} = \begin{cases} 2.8 \times 10^{-13} (L/L_\odot)^{1.5} & \text{if } (L/L_\odot) > 4.5 \\ 4.0 \times 10^{-37} (L/L_\odot)^{6.8} & \text{if } (L/L_\odot) < 4.5 \end{cases}.$$  (4)

These models yield very different X-ray luminosities for the case of the lower mass He-HMXBs which are expected to result from the observed Be-HMXBs. In this work, we use both Equations (3) and (4) and assess the effect on the observability of the He-HMXB population. We further note that both models depend on significant extrapolations from the wind strength of the presently observed WR population, and it is entirely possible that the actual wind strengths are significantly weaker than even Equation (4) would indicate. In this case, the observed population of He-HMXBs may be significantly smaller than determined here. In both cases, after applying the wind-mass loss rates, we follow Belczynski et al. (2008, Equations (39) and (83)) to calculate the X-ray luminosity of each individual system and to determine whether it enters the Chandra band.

Another uncertainty in this binary modeling concerns the evolutionary stage at which the Be-HMXB is observed, which affects how long the orbital evolution calculation should persist before the Be donor begins RLO. In order to constrain the error introduced by this uncertainty, we test three scenarios where current Be-HMXBs are assumed to be observed at zero-age main sequence (ZAMS), terminal-age main sequence (TAMS), and an intermediate case in the middle of the main-sequence lifespans (MAMS). This effectively brackets the uncertainty stemming from the evolutionary state of the observed Be-HMXB population. We note that the long orbital periods of Be-HMXBs rule out the possibility that this MS evolution is interrupted by CE phases prior to the formation of the NS component, as CEs are known to produce binaries with substantially shorter orbital periods than observed in any Be-HMXB system (Nebot Gómez-Morán et al. 2011).

In addition, we investigate the production of He-HMXBs from currently observed Be-HMXBs by expanding on this procedure through the creation of a grid containing systems with parameters similar to the observed Be-HMXB population. Specifically, we use the detailed stellar evolution code STARS to create a grid of stellar models with masses between 10 and 30 $M_\odot$ (with a resolution of 1 $M_\odot$) and a probability distribution following Salpeter (1955). We assume an initial orbital period in the range 10–200 days with a resolution of 1 day, and a density distribution which is flat in the logarithm of orbital period, which we use as a tracer for the orbital parameters (Abt 1983). In an alternative model we also investigate systems with orbital periods extending out to 400 days and 1000 days, to determine the impact of this cutoff on our results. Finally, we employ a thermal eccentricity distribution following Heggie (1975). From this grid, the probability of a given progenitor surviving to become a visible He-HMXB can be computed for an arbitrarily large population of likely progenitor systems. The normalization of the survivable probability to stellar environments can be ascertained through normalization against the observed number of Be-HMXBs as described in Section 4.
In Figure 1, we illustrate the dynamics of our orbital evolution code by providing the detailed evolutionary history for a single simulation of 0236+610 (Table 1). Specifically, we plot the code by providing the detailed evolutionary history for a single (A color version of this figure is available in the online journal.)

driving the system into spin–orbit synchronism. This mechanism controls the remaining orbital evolution leading to a decrease in the orbital separation and eccentricity, and increases the efficiency of tides. This mechanism sets an extremely conservative lower bound on the population of expected He-HMXBs, as it assumes that the Be-HMXB is X-ray bright for the entire MS lifetime of the donor star. This assumption is unrealistic, as it includes the portion of the MS lifetime during which the star is a Be-HMXB: its entire lifetime (black solid), beginning at 5 Myr (red dashed), beginning at 10 Myr (blue long dashed), and at the SN age of a primary star which is three times as massive as $M_{ZAMS}$ (green dot-dashed). The mass range of 2.5–4 $M_\odot$ for our population of He stars is set by the range of He core masses found in our models.

(A color version of this figure is available in the online journal.)

3. RESULTS FOR THE OBSERVED Be-HMXBs

In Figure 1, we illustrate the dynamics of our orbital evolution code by providing the detailed evolutionary history for a single simulation of 0236+610 (Table 1). Specifically, we plot the evolution in time of the orbital separation, eccentricity, stellar radius, Roche-lobe radius, spin, and orbital frequencies until the onset of RLO, when our calculation is halted. In this simulation we assume that the Be companion is currently observed at ZAMS.

From this detailed analysis it is evident that the evolution of the each parameter is dominated by only the last 0.1% of its total lifetime, when the star develops a convective envelope which strongly enhance the tidal evolution. This suggests that simulations beginning at ZAMS, MAMS, or TAMS will produce nearly identical binary parameters at the onset of the CE.

The currently observed population of Be-HMXBs includes only 13 systems with sufficient observational constraints to allow for a detailed modeling of their orbital evolution forward in time (listed in Table 1). Therefore, it is important to first determine which factors, other than CE dynamics, could prevent the observation of He-HMXBs. Taking a small step aside, we test two likely factors, the relative lifetime of a bright He-HMXB phase compared to the Be-HMXB phase and the expected X-ray luminosity of the He-HMXB population.

One possible explanation for the lack of observed He-HMXBs concerns the relative duration of He-HMXB and Be-HMXB phases. If the time the stellar component spends as an He star is only a small fraction of the Be-HMXB lifetime, we would be unlikely to observe a large population of these systems regardless of the CE dynamics. In order to investigate this effect, we follow the calculations of Hurley et al. (2000) where the lifetimes of the MS and He-MS phases ($\tau_{MS}$ and $\tau_{He}$, respectively) are given by

$$\tau_{MS} = \frac{1594 + 2707M_0^4 + 146.6M_0^{5.5} + M_0^7}{0.04142M_0^2 + 0.3426M_0^7} \text{Myr}$$

$$\tau_{He} = \frac{4.129 + 18.81M_0^4}{M_0^{5.5}} \text{Myr}$$

where $M_0$ is the ZAMS mass and $M_{He}$ is the mass of the He MS star. We note that the direct comparison of these lifetimes sets an extremely conservative lower bound on the population of expected He-HMXBs, as it assumes that the Be-HMXB is X-ray bright for the entire MS lifetime of the donor star. This assumption is unrealistic, as it includes the portion of the MS lifetime which occurs prior to the evolution of the primary star into an NS. In Figure 2, we plot the fractional lifetime for an He star of 2.5 $M_\odot$, 3 $M_\odot$, and 4 $M_\odot$ as a function of the ZAMS mass under four assumptions for the fraction of the total MS lifetime our observed systems spend as a Be-HMXB. First, we assume
that the system exists as a Be-HMXB for its entire MS lifetime. Second, we subtract 5 Myr from the MS lifetime to account for the formation of an NS from the most massive progenitors (see, e.g., Munro et al. 2006). Third, we subtract 10 Myr from the NS lifetime to account for the average lifetime of NS progenitors (Heger et al. 2003). Lastly, we follow the model of McSwain & Gies (2005), who propose that the early evolution of Be-HMXBs is governed by stable mass transfer from the NS progenitor onto the Be progenitor. This scenario sets an upper limit on the mass ratio between the primary and secondary stars at the onset of RLO based on the requirement that the accreting star achieves thermal equilibrium on a timescale smaller than the mass transfer timescale of the primary star. While the exact mass ratio may depend sensitively on the evolutionary state of each stellar component (Iben &Livio 1993), for MS companions Hjellming (1989) set a range of 2–4, while more recent work by Ivanova & Taam (2004) set a mass ratio of approximately 3. Motivated by these analyses, we lastly calculate the relative lifetime of the Be-HMXB phase as the MS lifetime of a Be star minus the MS lifetime of a progenitor star which is initially three times as massive. We note that all these scenarios are fairly conservative, due to the possibility that NSs in Be-HMXBs are formed via Electron-Capture supernovae (Nomoto 1984), which sets much stronger constraints on the lifetime of the Be-HMXB phase (Linden et al. 2009). We note that a range of 2.5–4 $M_\odot$ for the mass of the He core at the time of CE formation is strongly suggested by the results of our detailed stellar evolution models. 

Even considering the most massive He stars (with the shortest lifetime), as well as the most conservative calculation of the Be-HMXB lifetime, we expect a fractional lifetime ($t_{He}/t_{Fe}$) of between 5% and 10% for Be stars between 10 and 15 $M_\odot$. Thus, the population of 81 currently observed Be-HMXBs predicts a population of at least 6 Be-HMXBs, which is at odds with the observation of only one such system at the 2$\sigma$ level. A significantly larger population exceeding 15 He-HMXBs is expected from more reasonable calculations of the luminous Be-HMXB lifetime and the He rich stellar mass. Thus, we may reject the hypothesis that the lack of observed He-HMXBs stems from their short lifespan.

A second explanation for the lack of observed He-HMXBs concerns their assumed X-ray luminosities. If mass lost from the He star is not efficiently transferred onto the NS, the systems may simply fall below the luminosity threshold of present observations. In this work, we assume that any system with an X-ray luminosity in the Chandra band exceeding $1 \times 10^{34}$ erg s$^{-1}$ would have been detectable in galactic surveys (A. Zezas 2008, private communication). We note that this assumption is conservative, and based primarily on the sensitivity of X-ray survey missions such as ROSAT. A comparison with the X-ray luminosities of the Be-HMXB population shows several systems with detected luminosities below this level (Raguzova & Popov 2005).

We note that these calculations depend sensitively on both the mass of the He core determined by our evolutionary code, as well as the wind mass loss rate assigned to these systems. We find that our He stars span a mass range of approximately 2.5–4 $M_\odot$ with one outlier exceeding 6 $M_\odot$. In Figure 3, we plot the calculated X-ray luminosity as a function of the orbital period for He-HMXBs hosting an He stellar component with a mass of 2.5 $M_\odot$ (black), 3 $M_\odot$ (red), and 4 $M_\odot$ (blue), and following the wind mass-loss models of both Hurley et al. (2000) and Dewi et al. (2002) as given in Section 2. If stellar winds following the prescription of Hurley et al. (2000) are applied, these systems remain above the luminosity threshold out to orbital separations greatly exceeding those expected in post-CE binaries, which follow a logarithmic normal distribution spanning from 1.9 hr to 4.3 days, with a peak at 10.3 hr (Nebo Gómez-Morán et al. 2011). However, in the case of the weaker winds applied by Dewi et al. (2002), the final orbital separation of the systems may affect its detectability in the Chandra band.

Throughout what follows, we adopt the more conservative He mass-loss prescriptions of Dewi et al. (2002), and only count as "detectable" those He-HMXBs with a luminosity exceeding $1 \times 10^{34}$ erg s$^{-1}$.

Another process that might prevent He–NS binaries to be detected as X-ray sources is the propeller effect. It has been previously noted (Vanbeveren et al. 1999b) that a high rotational velocity for the NS accretor may prevent accretion of the donor wind material onto the NS. However, this is unlikely to affect the He-HMXB population modeled here. Since these systems are observed to be X-ray bright during the Be-HMXB phase, when the winds are less intense and the orbits are significantly wider, it is unlikely that the propeller effect will prevent the much stronger wind accretion during the tighter, post-CE phase. While the NS may be spun up during the CE phase, this spin-up is thought to be accompanied by a decrease in the NS magnetic field. Such an effect is indeed observed for the pulsars contained in double-NS systems which have moved through CE evolution. These systems are expected to exist as the offspring of the He-HMXB population, and their reduced magnetic fields allow at least quasi-periodic accretion onto the NS despite the high angular momentum in these NS (Romanova et al. 2004). In order to quantitatively examine the influence of the propeller effect on the He-HMXB population, a better understanding of NS spin and magnetic field evolution is required, but this is not possible at present.
Figure 4. Number of surviving and observable \((L_x > 10^{34} \text{ erg s}^{-1})\) He-HMXBs as a function of the CE parameter \(\alpha_{\text{CE}}\) employing the orbital characteristics at RLO determined via our stellar evolution code for the 13 known Be-HMXBs. (A color version of this figure is available in the online journal.)

3.2. CE and the Observed Be-HMXB Population

Since the He-HMXB population has both a sufficiently long lifespan and high luminosity to indicate the existence of numerous observable systems, another mechanism must halt the formation of these binaries. Since their progenitors are known to exist during the Be-HMXB phase, CEs stand as the only dynamical interaction which may eliminate He-HMXB progenitors. Thus, it is possible to set constraints on the CE efficiency \(\alpha_{\text{CE}}\) by demanding that enough of these systems are disrupted during a CE to bring the respective populations into agreement. Using the 13 Be-HMXBs with known orbital parameters as a template for the larger population of 81 systems and employing the detailed stellar evolution models calculated with STARS, we employ our orbital evolution code to determine the orbital and stellar parameters of the observed Be-HMXBs at the onset of the CE.

We again stress that we employ a calculation of \(|E_{\text{bind}}|\) which includes not only the gravitational energy necessary to eject the primary envelope, but additionally the thermal energy in the envelope as well as H2 association and reionization. Since no other significant energy sources are available, the value of \(\alpha_{\text{CE}}\) must fall below unity in order to conserve energy. In Figure 4, we show the number of surviving He-HMXBs as a function of the CE efficiency \(\alpha_{\text{CE}}\) under the assumption that detectable Be-HMXBs were observed at the ZAMS, MAMS, and TAMS, and with \(X_{\text{min}}\) set to 15%, 10%, and 1%. We find nearly identical results in all scenarios, indicating that for \(\alpha_{\text{CE}} \lesssim 1\), mergers occur in all 13 of the observed Be-HMXB systems, regardless of their previous evolutionary history. Since one He-HMXB is in fact observed, and the lifetime of He-HMXBs may be smaller than that of Be-HMXBs, our model is only able to constrain \(\alpha_{\text{CE}}\) to fall below unity, in line with theoretical expectations. We find that these results do indicate that current models are not missing any significant energy sources available to remove the CE, as the survivability of the CE phase exceeds 50% for \(\alpha_{\text{CE}} > 1.5\), and these systems would be observable even with the weakened wind prescriptions of Dewi et al. (2002).

4. A COMPLETE PARAMETER SPACE

In the previous sections, we have shown that CE-driven mergers are necessary to explain the discrepancy between Be-HMXB and He-HMXB observations and that the typical CE parameterization, which demands an efficiency less than unity when all possible energy sources for unbinding the envelope are accounted for, is consistent with the observed sample of only one He-HMXB. However, these observed Be-HMXBs exist only as a subset for the potential class of He-HMXB progenitors. In addition to these luminous systems, there may exist a much larger population of binaries containing an O/B star and an NS in wide orbits, such that they are not bright X-ray systems. This underlying population remains undetected because either the donor star does not carry enhanced winds stemming from the Be phenomenon or the system is too widely separated for stellar material to be effectively accreted onto the NS. In any case, the binary dynamics of this underlying population are identical to the visible population, and evolution through a CE phase may similarly result in bright He-HMXBs.

In order to model the evolution of these systems, we create a grid of binaries containing an NS and O/B donor following the parameters described in Section 2. In Figure 5, we show the fraction of binaries which survives the CE yielding bright He-HMXBs. We assume maximum initial orbital periods of 200 days (black solid), 400 days (blue dashed), and 1000 days (red dotted), following a distribution which is flat in the logarithm of the orbital period. We find that a potentially sizable fraction of He-HMXBs are created for larger values of \(\alpha_{\text{CE}}\), although the bounds depend strongly on the maximum assumed
orbital period of the underlying O/B–NS population. We note that the observation of two Be-HMXBs with orbital periods above 200 days allows us to set this as an observed lower limit for our simulated population (see Table 1). We also note that we do not expect a significant variation in our results if we were to vary the minimum orbital period in our sample grid (currently set at 10 days). These relatively tightly bound systems are unlikely to survive a CE, and their inclusion in our models will not greatly affect the calculated number of He-HMXBs.

In order to apply these results to the expected number of observed He-HMXBs, we must normalize the number of systems in our grid against the expected number of loosely bound O/B–NS binaries. We note that the number of He-HMXBs expected from our simulated population of O/B–NS systems can be expressed as

\[ N_{\text{He-HMXBs}} = f_s \left( \frac{N_{\text{Be}}}{N_B} \right)^{-1} \left( \frac{\tau_{\text{He}}}{\tau_{\text{He-HMXB}}} \right) N_O, \]

where \( f_s \) is the survival probability of a given system from our simulation grid (shown in Figure 5), \( N_{\text{Be}}/N_B \) provides the fraction of B-type donors which have Be-HMXB properties, \( \tau_{\text{He}}/\tau_{\text{He-HMXB}} \) describes the relative lifetime of the He-HMXB and Be-HMXB phases (shown in Figure 2), and \( N_O \) is the observed number of Be-HMXB systems (\( N_O = 81 \) throughout this paper).

The fraction of B-type stars which show emission-line (Be) spectra have been observed to vary between 2% and 7% (McSwain & Gies 2005), although we note some sources have shown Be-fractions as high as 8.5% (McSwain et al. 2008). While this ratio may be substantially higher in binary systems if the spin-up of the Be population is due to binary interactions, this line of reasoning is disputed by Oudmaijer & Parr (2010), who find a similar binary fraction for both B and Be stars. In this work, we assume a Be-fraction of 7%, and a fractional lifetime for the He-HMXB population (\( \tau_{\text{He}}/\tau_{\text{He-HMXB}} \)) of 20%, taking a central value from Figure 2 under the assumption that the primary progenitor was not more than three times as massive as the Be-star. We note that the X-ray detectability of these systems is evaluated for each surviving He-HMXB produced by our grid using the luminosity prescriptions of Dewi et al. (2002) and a luminosity cutoff of \( 1 \times 10^{33} \text{ erg s}^{-1} \). From these values, we would anticipate a population of 230\( f_s \) visible He-HMXBs.

Thus, we constrain \( f_s \) by comparing this expected population of He-HMXBs to the observation of only a single system. Noting that a prediction exceeding four He-HMXBs would create a 2σ discrepancy with observation, we thus constrain the survivability of the CE phase to less than 2%. Comparison with Figure 5 thus constrains the CE efficiency to \( \alpha_{\text{CE}} < 0.88 \), \( \alpha_{\text{CE}} < 0.75 \), and \( \alpha_{\text{CE}} < 0.50 \) if the maximum orbital period is 200 days, 400 days, and 1000 days, respectively.

We note that the above calculation is conservative in several ways. First, we have assumed that all systems containing a Be star and NS are visibly bright X-ray sources. Second, we have assumed that the observed population of Be-HMXBs can be translated to a population of O/B–NS with an orbital period which is logarithmically flat starting at 10 days. We note that the observed Be-HMXB population is instead biased toward systems with orbital periods around 100 days. While the lack of observed loosely bound systems may be due to luminosity cutoffs or simply limited to observational time, the low period population is likely complete. This implies that the survival fraction of O/B–NS systems resembling the Be-HMXBs may be substantially higher. However, less conservative estimations are unlikely to significantly alter the constraint imposed on the CE evolution, as Figure 5 shows that the survivability of the CE phase plunges for smaller values of \( \alpha_{\text{CE}} \), implying that uncertainties in the estimation of the population of O/B–NS binaries has only a negligible effect on the number of expected He-HMXBs.

5. DISCUSSION AND CONCLUSIONS

Theoretical models predict the production of He-HMXBs through the CE evolution of widely separated binaries containing an NS and a massive donor. However, observations show a large population of Be-HMXBs and a significant lack of He-HMXBs. We find that detailed theoretical models predict the He-HMXB population to be sufficiently long-lived and luminous to be detected as the evolved offspring of the observed Be-HMXB population. Noting that a CE phase acts as the only dynamical mechanism which may disrupt the production of He-HMXBs, we use these observations to set constraints on the CE efficiency parameter \( \alpha_{\text{CE}} \).

Using the binary parameters of the observed Be-HMXBs, we are only able to limit \( \alpha_{\text{CE}} \) to fall below unity, echoing theoretical constraints due to conservation of energy. Next, we simulate a larger grid of O/B–NS binaries with characteristics similar to the observed Be-HMXB population. From this grid, we constrain \( \alpha_{\text{CE}} \) to be <0.88 for a population of O/B–NS binaries with a maximum orbital period of 200 days, and possibly as low as \( \alpha_{\text{CE}} < 0.50 \) if the period extends to 1000 days. We note that this extension of the O/B–NS population to high orbital periods may have observational support, as one X-ray quiet system (B1259-63) with an orbital period of 1236 days has been observed as a radio pulsar with an optically identified B-type companion (Hughes & Bailes 1999; Wex et al. 1998).

We note that the stringency of our constraints is limited primarily by the low number of observed Be-HMXBs, and especially by the limited number of Be-HMXBs with known orbital period and eccentricity information. We expect that observational detections of both new B-star NS binaries and determinations of the binary parameters of known Be-HMXBs will greatly reduce these measurement errors and provide a more accurate understanding of CE evolution in massive binaries. Furthermore, we note that our findings are complementary to previous studies which employ a combination of natal kicks and/or CE mergers to explain the small population of He-HMXBs with more massive (\( M_{\text{He}} > 5 M_\odot \)) helium donors (De Donder et al. 1997; Vanbeveren et al. 1998a; Lommen et al. 2005). Specifically, we extend the analysis to the lower mass range of He-HMXBs formed through the evolution of the Be-HMXB population and then use the number and binary properties of the observed Be-HMXBs to determine the natal kick and CE merger hypotheses. We find that independent of any disruptions due to natal kicks (which would occur prior to the Be-HMXB phase), CE mergers must be common in order to explain the relative paucity of He-HMXBs. Using this, we can place strict limits on the CE efficiency.

Lastly, we note that a similar methodology may be applied to the population of known NS–NS binaries containing a pulsar, in order to determine whether the rate of NS–NS production is itself consistent with the low survivability probability assigned to Be-HMXBs moving through CE phases. Since these systems would additionally experience an He-HMXB phase in between the Be-HMXB and NS–NS phases, the existence of a large NS–NS population inconsistent with the small number of Be-HMXBs would instead point toward the existence of an
X-ray quiet population of He-HMXBs, and may be used as a further test of the results obtained here.

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REFERENCES

Abt, H. A. 1983, ARA&A, 21, 343
Bailyn, C. D., & Grindlay, J. E. 1987, ApJ, 316, L25
Belczynski, K., Kalogera, V., Rasio, F. A., et al. 2008a, ApJS, 174, 223
Belczynski, K., & Ziołkowski, J. 2009, ApJ, 707, 870
Bondi, H., & Hoyle, F. 1944, MNRAS, 104, 273
Chevalier, C., & Ilovaisky, S. A. 1998, A&A, 330, 201
Claret, A. 2004, A&A, 424, 919
Corbet, R. H. D., & Krimm, H. A. 2009, ATel, 2008, 1
De Donder, E., Vanbeveren, D., & van Bever, J. 1997, A&A, 318, 812
de Jager, C., Nieuwenhuijzen, H., & van der Hucht, K. A. 1988, A&A, 72, 259
Dewi, J. D. M., Pols, O. R., Savonije, G. J., & van den Heuvel, E. P. J. 2002, MNRAS, 331, 1027
Dewi, J. D. M., & Tauris, T. M. 2000, A&A, 360, 1043
Eggleton, P. P. 1971, MNRAS, 151, 351
Eggleton, P. P. 1973, MNRAS, 163, 279
Eggleton, P. P., & Kiseleva-Eggleton, L. 2002, ApJ, 575, 461
Eggleton, P. P., & Verbunt, F. 1986, MNRAS, 220, 13P
Hamann, W.-R., & Koesterke, L. 1998, A&A, 335, 1003
Hamann, W.-R., Koesterke, L., & Wessolowski, U. 1995, A&A, 299, 151
Han, Z., Pols, O. R., & Eggleton, P. P. 1994, MNRAS, 270, 121
Han, Z., Podsiadlowski, P., & Eggleton, P. P. 1995, MNRAS, 272, 800
Heger, A., Fryer, C. L., Woosley, S. E., Langer, N., & Hartmann, D. H. 2003, ApJ, 591, 288
Heggie, D. C. 1975, MNRAS, 173, 729
Hjellming, M. S. 1989, PhD thesis, Illinois Univ. Urbana-Champaign, Savoy
Hughes, A., & Bailes, M. 1999, ApJ, 522, 504
Hurley, J. R., Pols, O. R., & Tout, C. A. 2000, MNRAS, 315, 543
Hurley, J. R., Tout, C. A., & Pols, O. R. 2002, MNRAS, 329, 897
Hut, P. 1981, A&A, 99, 126
Iben, I., Jr., & Livio, M. 1993, PASP, 105, 1373
Ivanova, N., & Taam, R. E. 2004, ApJ, 601, 1058
Junkes, W., & Schaefer, G. 1992, MNRAS, 254, 146
Kaur, R., Paul, B., & Sagar, R. 2008, MNRAS, 386, 2253
Kaufman, J., Sepinsky, J. F., Kalogera, V., & Belczynski, K. 2009, ApJ, 699, 1573
Lommen, D., Yungelson, L., van den Heuvel, E., Nelemans, G., & Portegies Zwart, S. 2005, A&A, 443, 231
Loveridge, A. J., van der Sluys, M., & Kalogera, V. 2011, ApJ, 743, 49
McSwain, M. V., & Gies, D. R. 2005, ApJS, 161, 118
McSwain, M. V., Huang, W., Gies, D. R., Grundstrom, E. D., & Townsend, R. H. D. 2008, ApJ, 672, 590
Moffat, A. F. J., Firmani, C., McLean, I. S., & Seggewiss, W. 1982a, in IAU Symp., 99, Wolf–Rayet Stars: Observations, Physics, Evolution, ed. C. W. H. De Loore & A. J. Willis (Cambridge: Cambridge Univ. Press), 577
Moffat, A. F. J., Lamontagne, R., & Seggewiss, W. 1982b, A&A, 114, 135
Muno, M. P., Clark, J. S., Crowther, P. A., et al. 2006, ApJ, 636, L41
Nebot Gómez-Morán, A., Gansicke, B. T., Schreiber, M. R., et al. 2011, A&A, 536, A43
Nelemans, G., & van den Heuvel, E. P. J. 2001, A&A, 376, 950
Nomoto, K. 1984, ApJ, 277, 791
Nugis, T., & Lamers, H. J. G. L. M. 2000, A&A, 360, 227
Oudmaijer, R. D., & Parr, A. M. 2010, MNRAS, 405, 2439
Paczynski, B. 1976, in IAU Symp. 73, Structure and Evolution of Close Binary Systems, ed. P. Eggleton, S. Mitton, & J. Whelan (Cambridge: Cambridge Univ. Press), 75
Pols, O. R., Tout, C. A., Eggleton, P. P., & Han, Z. 1995, MNRAS, 274, 964
Raguzova, N. V., & Popov, S. B. 2005, Astron. Astrophys. Trans., 24, 151
Rasio, F. A., & Livio, M. 1996, ApJ, 471, 366
Ricker, P. M., & Taam, R. E. 2008, ApJ, 672, L41
Rodriguez, J., Tomskis, J. A., & Bodaghee, A. 2010, A&A, 517, A14
Rodriguez, J., Tomskis, J. A., & Chatty, S. 2009, A&A, 494, 417
Romanova, M. M., Ustyugova, G. V., Koldoba, A. V., & Lovelace, R. V. E. 2004, ApJ, 616, L151
Salpeter, E. E. 1955, ApJ, 121, 161
Sandquist, E. L., Taam, R. E., & Burkert, A. 2000, ApJ, 533, 984
Sepinsky, J. F., Willems, B., & Kalogera, V. 2007, ApJ, 660, 1624
Taam, R. E., & Ricker, P. M. 2006, arXiv:astro-ph/0611043
Taam, R. E., & Sandquist, E. L. 2000, ARA&A, 38, 113
Van Bever, J., & Vanbeveren, D. 2000, A&A, 358, 462
van den Heuvel, E. P. J. 1976, in IAU Symp. 73, Structure and Evolution of Close Binary Systems, ed. P. Eggleton, S. Mitton, & J. Whelan (Cambridge: Cambridge Univ. Press), 35
van den Heuvel, E. P. J., Portegies Zwart, S. F., Bhattacharya, D., & Kaper, L. 2000, A&A, 364, 563
van der Sluys, M., Kalogera, V., & Belczynski, K. 2009, ApJ, 699, 1573
van der Sluys, M., Kalogera, V., & Belczynski, K. 2009, ApJ, 699, 1573
van Kerkwijk, M. H., Charles, P. A., Geballe, T. R., et al. 1992, Nature, 355, 703
Vanbeveren, D., De Donder, E., van Bever, J., & Rensbergen, W., & De Loore, C. 1998a, New Astron., 3, 443
Vanbeveren, D., De Loore, C., & Van Rensbergen, W. 1998b, A&A, 9, 63
Webbink, R. F. 1984, ApJ, 277, 355