The Solar Cycle Temporal Variation of the Solar Wind Charge Exchange X-Ray Lines

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Abstract

Solar wind charge exchange (SWCX) is the primary contamination of soft X-ray emission lines from the Milky Way (MW) hot gas. We report a solar cycle (∼10 yr) temporal variation of observed O VII and O VIII emission line measurements in the XMM-Newton archive, which is tightly correlated with the solar cycle traced by the sunspot number (SSN). This temporal variation is expected to be associated with the heliospheric SWCX. Another observed correlation is that higher solar wind (SW) fluxes lead to higher O VII or O VIII fluxes, which is due to the magnetospheric SWCX. We construct an empirical model to reproduce the observed correlation between the line measurements and the solar activity (i.e., the SW flux and the SSN). With this model we discovered a lag of 0.91 ± 0.23 yr between the O VII flux and the SSN. This time lag is a combination of the SW transit time within the heliosphere, the lag of the neutral gas distribution responding to solar activity, and the intrinsic lag between the SSN and the launch of a high-energy SW (i.e., O7+ and O8+). MW O VII and O VIII fluxes have mean values of 5.4 L.U. and 1.7 L.U., which are reduced by 50% and 30%, compared to studies where the SWCX contamination is not removed. This correction also changes the determination of the density distribution and the temperature profile of the MW hot gas.

Unified Astronomy Thesaurus concepts: Solar wind (1534); Circumgalactic medium (1879); Charge exchange ionization (2056); Milky Way Galaxy (1054)

1. Introduction

The soft X-ray emission traces the hot gas with $T \approx 10^6$ K, which is predicted to dominate the baryons in the local Universe (Cen & Ostriker 1999; Bregman 2007). Previous studies revealed that the Milky Way (MW) hosts a gaseous halo with $T \approx 2 \times 10^6$ K (e.g., Henley & Shelton 2010; Kaaret et al. 2020). However, a long-term issue of MW X-ray studies is the foreground contamination due to the solar wind charge exchange (SWCX), which is induced when the solar wind (SW) interacts with the neutral gas within the heliosphere. The SWCX is identified as an efficient mechanism of soft X-ray line emission (Cravens 1997) and contaminates measurements of the O VII and O VIII fluxes of the MW hot gas (Henley & Shelton 2013).

There are two types of SWCX distinguished by different origins of the neutral gas interacting with the SW (see Kuntz 2019 for a review). First, the neutral gas in the Earth’s atmosphere could interact with the SW, which is known as the magnetospheric SWCX, because it happens in the magnetosphere of the Earth. This emission was discovered as the long-term enhancements (LTEs; variation over days) by ROSAT in the soft X-ray band (Cravens et al. 2001). Because this SWCX happens near the Earth, there is no obvious lag between the temporal variation of the local SW flux around the Earth and the observed soft X-ray enhancement.

Another origin of the neutral gas is the interplanetary medium (IPM) within the heliosphere, which leads to the heliospheric SWCX. Using deep X-ray observations, Koutroumpa et al. (2007) found that the O VII (O VIII) heliospheric SWCX has a large variation from 0.3 to 4.6 (0.02–2.1) L.U. (line units; counts s$^{-1}$ cm$^{-2}$ sr$^{-1}$). Henley & Shelton (2012, hereafter HS12) found that the SWCX (mainly heliospheric) O VII and O VIII fluxes are $\lesssim 5$ L.U. and $\lesssim 2$ L.U. using multiple epochs of observations of the same sightline in the XMM-Newton archive.

However, the temporal behavior of the heliospheric SWCX is still uncertain. The temporal variation depends upon the distribution of the neutral gas, the propagation of the solar wind through the heliosphere, and the way that the solar wind modifies the distribution of neutral gas. Some studies have performed detailed calculations of the SWCX on a per observation basis and used those estimates to subtract the SWCX contamination from the Galactic O VII and O VIII emission (e.g., Kaaret et al. 2020). However, this was not performed for the widely used O VII and O VIII line survey of HS12 (i.e., the current largest and highest spatial resolution sample for the MW and SWCX studies). In this letter, we investigate both types of SWCX empirically using the O VII and O VIII line survey (HS12) and report evidence for a long-term temporal variation of the SWCX. We constructed an empirical model to reproduce the observed correlation between O VII and O VIII line measurements and solar activity (e.g., the SW flux measured around the Earth and the sunspot number; SSN). This model provides a sample of Galactic O VII and O VIII emission that has been far better cleaned of SWCX contamination than previous studies (using the HS12 survey).
2. Data and Observed Correlations

In this study we adopted the data from HS12, which reduced all archived XMM-Newton observations prior to 2010 August 4. HS12 measured the OVII and OVIII line fluxes by disabling their emissions in APEC or MEKAL models (Mewe et al. 1985; Kaastra & Jansen 1993; Smith et al. 2001) and adding two Gaussian emission lines to extract net line fluxes. They adopted three steps to reduce contamination after masking out solar flares. First, they masked out point sources with 0.5–2.0 keV flux $> F_{0.5-2.0} \approx 5 \times 10^{-14}$ erg cm$^{-2}$ s$^{-1}$ in the Second XMM-Newton Serendipitous Source Catalog (Watson et al. 2009) and extended sources by visual inspection. Second, they filtered out observations with high extragalactic power-law fluxes at 2–5 keV to exclude strong contamination from remaining point sources in the field, which resulted in a sample of 1868 sightlines. Third, the local SWCX contamination is reduced by filtering out periods with high local SW proton fluxes $> 2 \times 10^8$ counts cm$^{-2}$ (around the Earth obtained from the OMNIWeb database; King & Papitashvili 2005), which reduces the sample size to 1003.

However, these steps do not ensure that the SWCX is entirely removed in the HS12 low SW flux sample. In Figure 1, we divide the full sample of 1868 sightlines into two subgroups based on the median of the SW flux. The high SW flux sample leads to higher OVII fluxes with a median of 6.42 ± 0.16, while the low SW flux sample has a median of 5.57 ± 0.16, which is a 3.7σ difference. The $p$-value is $1.1 \times 10^{-7}$ in the Kolmogorov–Smirnov (KS) test. For OVIII, the median values of 1.35 ± 0.07 and 1.25 ± 0.09 for high and low SW samples, respectively. This is a 0.8σ difference and the KS test $p$-value is 0.29. This dependence of OVII and OVIII fluxes on the local SW flux is evidence for the magnetospheric SWCX (Cravens et al. 2001).

The heliospheric SWCX also introduces significant features in the HS12 sample. We resample the OVII and OVIII line fluxes based on the observation date in bins of six months in Figure 1. There is a significant decline of the OVII and OVIII line fluxes from 2000 to 2010. A KS test shows a $p$-value of $3.8 \times 10^{-13}$ on the two subsamples divided by the observation date of 2005 for both OVII and OVIII, which suggests a significance $> 10\sigma$. The peak of the OVII flux is about 8 L.U. in 2002, and the minimum is about 4 L.U. around 2009. This variation matches the solar cycle represented by the SSN, which has a maximum around 2000–2003, and a minimum around 2008. Therefore, we suggest that this solar cycle variation of the OVII and OVIII fluxes is evidence for the magnetospheric SWCX. We also note that this long-term heliospheric SWCX variation over years is different from the previously known LTE (i.e., the magnetospheric SWCX).
because the average SW flux at the Earth does not vary significantly from 2000 to 2010 (Figure 1).

3. An SWCX Empirical Model

We constructed an empirical model of the overall SWCX variation in order to remove the bulk of the SWCX emission from the XMM-Newton observations and to produce cleaner measures of the emission due to the MW hot halo. We model the variation in the two types of SWCX using their expected behavior. The magnetospheric SWCX is expected to be proportional to the SW flux, while the heliospheric SWCX is expected to be a function of solar activity.

The O VII and O VIII SWCX lines are produced by charge exchange with O$^{7+}$ and O$^{8+}$ in the SW. The density of those two ions within the line of sight depends upon both the SW flux (typically given as the proton flux) and the relative abundances of the ions with respect to the protons. Those abundances are a function of solar activity (e.g., the slow solar equatorial flow or the fast solar polar flow). The slow flow has higher O$^{7+}$ and O$^{8+}$ abundances than the fast flow (Kuntz 2019). During the solar cycle, the two flows are distinctly segregated, while at the solar maximum, the flows are intermixed. Thus, the overall properties of the O$^{7+}$ and O$^{8+}$ abundance will vary with the solar cycle. While some measures of SW O$^{7+}$ and O$^{8+}$ fluxes have been available from ACE, they do not have high signal-to-noise ratios, and those measures are representative of the solar equatorial flow around the Earth, which will be different from the solar polar flow. Therefore, we do not use the O$^{7+}$ and O$^{8+}$ fluxes in the empirical model.

The magnetospheric SWCX (e.g., the ROSAT LTE strength) is closely correlated with the SW flux around the Earth (Cravens et al. 2001; Kuntz et al. 2015). Figure 1 reiterates this dependence, showing that the O VII and O VIII line strengths are greater for observations during high SW flux periods than for observations during low SW flux periods. Therefore, in the empirical model, we assume that the magnetospheric SWCX is proportional to the local SW flux.

The heliospheric SWCX depends upon the observing line of sight (through the equatorial flow or the polar flow). These solar flows have dependences on the solar cycle (e.g., weaker polar flows at the solar minimum; McComas et al. 2008). The standard measure of solar activity within the solar cycle is the SSN, which is tightly correlated with a number of other properties of the solar cycle, such as the magnetic field (Smith et al. 2014). Therefore, we assume that the heliospheric SWCX is proportional to the SSN. We note that, as the SW flux is weakly correlated with the SSN, our measures of the magnetospheric and heliospheric SWCX are not entirely decoupled. However, this effect will not be noticeable in the following analysis.

For the heliospheric SWCX, we first smooth the SSN curve with a Gaussian function of $\sigma = 1$ yr to reduce the uncertainty introduced by the scattering and intercycle periodicity of the SSN (periods up to half a year; Joshi et al. 2006). The inclusion of the 1 yr smoothing factor will not change the long-term SSN variation, because the SSN peak can be approximated by a Gaussian with a width of $\approx 3$ yr. The additional 1 yr smoothing only increases the width by <5%, which cannot be distinguished by the current data. Our formulation also allows a lag ($\tau$) between the SSN and observed O VII and O VIII SWCX. This lag has three possible physical origins discussed in Section 4.1.

The contribution by the MW to the O VII and O VIII fluxes is nonnegligible. The MW contribution depends on the Galactic coordinates, showing a dependence on the angular separation to the Galactic center (GC; Figure 1), but does not have any dependence on the solar cycle or the local SW flux. Therefore, there is no correlation expected between the MW contribution and the magnetospheric or heliospheric SWCX. We assume a constant value for the Galactic contribution to the O VII and O VIII emission for this temporal analysis. The spatial distribution of MW hot gas emission will be discussed in Section 4.3. In this study we mask out sightlines with HI column densities $>2 \times 10^{21}$ cm$^{-2}$ (adopted from the HI4PI survey; Collaboration et al. 2016) in the final sample with 1602 observations. These sightlines are at low Galactic latitudes, often crossing bright structures, and contain emission that is different than the hot halo emission at higher Galactic latitudes.

Thus, the empirical model has three components. The observed O VII and O VIII are calculated as

$$I_m = A_{\text{mag}}F_{\text{SW}} + B_{\text{helio}}f(N_{\text{SSN}}, \sigma, \tau) + I_{\text{MW}},$$

where $F_{\text{SW}}$ is the local SW flux (adopted from HS12) for individual observations, and $f(N_{\text{SSN}}, \sigma, \tau)$ is the smoothed ($\sigma$) and lagged ($\tau$) SSN. The normalization factors ($A_{\text{mag}}$, $B_{\text{helio}}$, and $I_{\text{MW}}$ for magnetospheric, heliospheric, and MW, respectively) are different for O VII and O VIII, but we assume that O VII and O VIII share the same lag time ($\tau$). Therefore, in the empirical model, there are seven free parameters and one fixed parameter (smoothing width $\sigma = 1$ yr).

We adopt the Bayesian optimization to obtain the best parameters in the model. Specifically, the likelihood is calculated using the residuals in the logarithmic scale, because both the MW residual and the SWCX scatter are expected to be lognormal:

$$\ln p = \sum \frac{(\log I - \log I_m)^2}{\sigma_m^2 + \sigma_p^2} - \frac{1}{2} \ln(\sigma_m^2 + \sigma_p^2),$$

where $I$ is the observed O VII or O VIII line emission measurement, and $I_m$ is the model defined in Equation (1). The observational uncertainty ($\sigma_m$) is adopted from HS12, which is calculated by combining the systematic uncertainty and the measurement uncertainty. The parameter $\sigma_p$ is an empirical patchiness parameter to account for the scatter in residuals (mainly due to the MW spatial variation), which is different for O VII and O VIII.

The best parameters are obtained with emcee (Foreman-Mackey et al. 2013; shown in Figure 2). The fitted scaling relations for the magnetospheric and heliospheric SWCX O VII or O VIII are

$$I_{O7,\text{mag}} = (0.50 \pm 0.06)F_{\text{SW,8}},$$
$$I_{O8,\text{mag}} = (0.04^{+0.03}_{-0.02})F_{\text{SW,8}},$$
$$I_{O7,\text{helio}} = (2.11^{+0.14}_{-0.15})f(N_{\text{SSN}}, \sigma, \tau),$$
$$I_{O8,\text{helio}} = (0.57 \pm 0.08)f(N_{\text{SSN}}, \sigma, \tau),$$
$$I_{O7,\text{MW}} = 3.51^{+0.19}_{-0.18},$$
$$I_{O8,\text{MW}} = 1.28 \pm 0.09,$$

where $F_{\text{SW,8}}$ is the SW proton flux in units of $1 \times 10^8$ count s$^{-1}$. The smoothing timescale is fixed to one year, and the lag is
\( t = 0.91^{+0.20}_{-0.22} \) yr (11.2 months), which differs from zero at \( 4\sigma \) significance.

4. Implication and Discussion

4.1. The Lag between the SSN and the SWCX

In Figure 3, we scale the SSN to match the observed OVII flux and show this lag. This lag is dominated by OVII, while O VIII is too uncertain to determine the lag itself.

There are three possible origins for this lag. First, the heliospheric SWCX is expected to have a lag due to the transit time for the SW to reach the heliosphere. The radius of the heliosphere is about 120 au (Richardson et al. 2019), so the transit time of the SW is about 1.4 yr to reach the heliopause, considering the typical SW velocity of 400 km s\(^{-1}\). More accurate estimation of the transit time for the SWCX involves the neutral gas distribution, which suggests that \( >80\% \) of SWCX emission are within 20 au (Kuntz 2019), which leads an SW transit time of 0.2–0.3 yr.

Second, recent studies have revealed that the neutral gas distribution is nonstationary showing corresponding variation with the SW propagation (Koutroumpa et al. 2021). Increased SW flux could sweep up or ionize the neutral gas close to the Sun. The variation of the neutral gas density distribution leads
to a temporal variation of the integration of the neutral gas, which lags behind the SW variation, and further increases the lag between the SSN and the SWCX.

The third possibility is that there is an intrinsic lag between the SSN and the high ionization state ion flux in the SW corresponding to the solar cycle. Previous studies confirmed \( \approx 1-15 \) month lags between different tracers of the solar cycle (e.g., Bachmann & White 1994; Temmer et al. 2003; Ramesh & Vasantharaju 2014). It is possible that the high-energy solar activities generating O\(^{7+}\) and O\(^{8+}\) intrinsically lag the SSN, which accounts for an extra lag other than the transit time.

4.2. Earth Position-related Variation

There is an Earth position-related (seasonal) variation of the O\(^{7+}\) sample in the XMM-Newton archive, while the O\(^{8+}\) sample does not show this variation due to its lower signal-to-noise ratio. This seasonal variation is regulated by two factors. First, the neutral IPM is anisotropic due to the solar motion relative to the nearby interstellar medium (Baranov & Malama 1993; Opher et al. 2020). The upwind direction is roughly near the GC direction \((l, b) = (3^\circ, 16^\circ)\). In this direction, the neutral gas forms a high hydrogen density region (Lallement et al. 1984). In the downwind direction, although the hydrogen density is relatively lower, the helium density is enhanced due to the gravitational focusing of helium by the Sun, which is effective because of the higher mass of helium (Dalaudier et al. 1984). These over-dense regions lead to higher SWCX emissivities when the Earth passes through them. Thus, the heliospheric SWCX will have a seasonal variation that is closely aligned with the Galactic center/anticenter axis. Second, XMM-Newton mostly observes targets within \( \pm 10^\circ \) perpendicular to the Sun–Earth direction (selection of ecliptic longitudes), which is required to ensure sufficient energy supply and thermal stability of the spacecraft. Therefore, the observation pointing directions also have seasonal variation.

This seasonal variation is not considered in the empirical model, and, indeed, is mostly removed by our six-month binning. Instead, we examine and correct this seasonal variation using the residual of the empirical model after subtracting the long-term temporal variation of the two modeled SWCX components and the MW contribution. The two SWCX components are calculated from the empirical model. The MW contribution is not the constant value in the empirical model; instead, we calculate a position-dependent MW contribution.

We consider the spatial distribution of the MW hot halo emission, after subtracting the SWCX empirical models and correcting for the absorption (\texttt{phabs} absorption in \texttt{XSPEC}). The MW O\(^{7+}\) and O\(^{8+}\) line fluxes have a strong dependence on the angular distance to the GC (e.g., Miller & Bregman 2015). Therefore, the MW contribution is calculated as the interpolation of the angular radial profile related to the GC. For this empirical MW model, we consider the north–south asymmetry, where the northern sky is brighter than the southern sky by about 1 L.U. (Qu et al. 2021). Here, the empirical MW model still has contributions from the seasonal variation of the heliospheric SWCX, because the seasonal variation is not included in the empirical SWCX model. This seasonal variation has a nonzero mean, so this MW model is overestimated, which will be corrected in Section 4.3.

In Figure 4, we show the seasonal variation of the three empirical model components. The MW and the heliospheric SWCX have significant seasonal variations (>3\(\sigma\)), while the magnetospheric SWCX is a constant within uncertainty. First, the seasonal variation of the MW contribution is dominated by the XMM-Newton observing constraints, which sample different distances from the GC at different times of year (panel B in Figure 4). Second, for the heliospheric SWCX model, we do not expect temporal variations shorter than one year (including the seasonal variation), because the SSN is smoothed with one year in the empirical model. However, we find that the average observation dates in different seasonal bins are not constant (Figure 4), which leads to the observed seasonal variation for the heliospheric SWCX. From 2000 to 2010, the solar activity evolved from its maximum to its maximum.
minimum, so a later average observation date leads to a lower heliospheric SWCX (panel C in Figure 4). Third, the magnetospheric SWCX does not show a seasonal variation, as expected (panel D in Figure 4). The X-ray and soft proton flare filter in HS12 data reduction also filter out high local SW flux periods, which leads to the flat magnetospheric SWCX.

The final residual of O VII $I_{\text{total}} - (I_{\text{mag}} + I_{\text{helio}} + I_{\text{MW}})$; panel A-(B+C+D) in Figure 4] is shown in the last panel in Figure 4, which shows a tentative ($\approx 3\sigma$) seasonal variation. This seasonal variation has two peaks at the seasonal phase of 0.35 and 0.85, which are close to the upwind (0.42) and downwind directions (0.92). The upwind peak is slightly stronger than the downwind peak. We adopt a normalized simulation model (see the Appendix) to examine whether this observed seasonal variation in the residuals is the seasonal variation of the heliospheric SW. This simulation model only accounts for the neutral gas distribution, while the variation in the O$^{7+}$ SW flux is not included in this model. This normalized model is scaled to match the observed residual with an offset of $1.2 \pm 0.7$ L.U., which is the average heliospheric SWCX (within 1$\sigma$ of the empirical model of $1.8 \pm 0.3$ L.U.). We suggest that the observed residual is the seasonal variation of the heliospheric SWCX.

This seasonal variation residual varies from $-0.3$ to $+0.3$ L. U. (Figure 4). However, this residual seasonal variation should have a nonnegative minimum instead of $-0.3$ L. U. in Figure 4, because the empirical heliospheric SWCX model does not include this seasonal variation. Therefore, an average flux of $\approx 0.3$ L.U. has been attributed to the current MW empirical model, which will be corrected in Section 4.3.

4.3. The SWCX Clean MW Hot Gas Emission

The MW hot halo emission extracted in Section 4.2 is still contaminated by the heliospheric SWCX seasonal variation. To correct this contamination, we subtract another 0.3 L.U. together with observed residual seasonal variations from the MW emission.

In Figure 5, we show the MW hot gas emission before and after the SWCX correction. The average MW fluxes are reduced by 50% for O VII (the mean of 10.0 L.U. to 5.4 L.U.) and 30% for O VIII (2.5 L.U. to 1.7 L.U.), compared to previous studies where the SWCX component is not accounted for.
An order-of-magnitude estimation suggests that the MW hot gas mass is overestimated by 20%–30%. Furthermore, the SWCX correction is more important in the outskirts, where the MW emission is low. Previously, the MW hot gas distribution (within 50 kpc) is determined to be a power law with a slope of 1.2–1.5 by assuming a constant temperature of $2 \times 10^6$ K (Miller & Bregman 2015; Li & Bregman 2017). For both O VII and O VIII, our new samples have a steeper decline, which determines the hot gas density distribution, and will further reduce the mass that may be hosted at large radii.

The SWCX correction also changes the temperature determination. The MW hot gas temperature is declining from the inner region dominated by the hot gas bubbles Fermi and eROSITA bubbles to the outskirts (Su et al. 2010; Miller & Bregman 2016; Predehl et al. 2020). The O VIII/O VII ratio, as the tracer of the temperature, varies from about 0.6–0.7 (inner 20°) to about 0.1–0.2 (outskirts). In the empirical model, the SWCX O VIII/O VII ratio is 0.20$^{+0.03}_{-0.06}$. Therefore, the temperature is underestimated in the inner region and overestimated in the outskirts of the SWCX contribution is not accounted for. In the lower panel Figure 5, we show the ratio of the O VIII/O VII ratio before and after the SWCX correction, which shows a transition point at 80° for the temperature correction. Another trend is that the ratio increases again beyond 120°. This increase indicates that with a higher temperature around the MW disk, as the angular separation increases, the selected region will be more and more concentrated in the anti-GC direction in the disk.

The SWCX correction of the HS12 sample improves the determination of both density distribution and the temperature profile of the MW hot gas. The detailed modeling of the MW hot gas will be presented in a future work.

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Appendix

The SWCX emissivity depends on the neutral gas distribution within the heliosphere and the strength of the high-energy SW (i.e., $O^{7+}$ and $O^{8+}$). The SWCX reaction between SW ions...
\(X^{q+} + \text{heliospheric neutrals N (H or He)} \rightarrow X^{(q-1)+} + \text{N}^+ + \gamma\).

In this work, we focus on oxygen ions \((X = O)\) for parent charge states \(q = 7, 8, \) and \(\gamma\) refers to the resulting O VII triplet \((E \approx 0.57 \text{ keV})\) and O VIII Ly\(\alpha\) \((E \approx 0.65 \text{ keV})\) lines, respectively.

The simulated total flux along the line of sight is calculated as:

\[
I = \frac{1}{4\pi} \int_{\beta=0}^{\infty} F_{X^{q+}}(R)[n_H(\lambda, \beta, R)\sigma_H^{X^{q+}} Y_H^{X^{q+}}
+ n_{He}(\lambda, \beta, R)\sigma_{He}^{X^{q+}} Y_{He}^{X^{q+}}]ds, \tag{A1}
\]

where \(F_{X^{q+}}(R) = F_{X^{q+}}(1 \text{ au}) \times (1 \text{ au}/R)^2\) is the ion flux depending on the radial distance to the Sun \((R)\), and \(n_N(\lambda, \beta, R)\) is the neutral density for H and He in the interplanetary space, dependent on the direction in ecliptic coordinates \((\lambda, \beta)\), and \(R\). The parameter \(\sigma_N^{X^{q+}}\) is the SWCX cross section for reactions between ion \(X^{q+}\) and neutral N, and \(Y_N^{X^{q+}}\) is the corresponding line emission probability following the specific SWCX reaction.

The high-energy ion flux \(F_{X^{q+}}(1 \text{ au})\) has large uncertainties because only the in situ flux can be measured at 1 au by current instruments. Therefore, we isolate the ion flux from the SWCX calculation in the Equation (2), and define the normalized model:

\[
Q = \frac{1}{4\pi} \int_{\beta=0}^{\infty} \frac{1}{R^2}[n_H(\lambda, \beta, R)\sigma_H^{X^{q+}} Y_H^{X^{q+}}
+ n_{He}(\lambda, \beta, R)\sigma_{He}^{X^{q+}} Y_{He}^{X^{q+}}]ds. \tag{A2}
\]

The neutral density calculations \(n_N(\lambda, \beta, R)\) are detailed in Koutroumpa et al. (2006), based on models by Lallement et al. (1984) for H and Dalaudier et al. (1984) for He.

The distributions are calculated by following the particle trajectories in the heliosphere, assuming they form a parallel flow with a Maxwellian velocity distribution after crossing the heliopause. The local neutral density in interplanetary space is calculated based on solar activity and loss processes depending on the solar cycle phase. Hydrogen trajectories are dominated by the ratio \(\mu\) of solar radiation pressure to gravity \((\mu > 1)\) for the solar maximum, and \(<1\) for the solar minimum. Loss processes for hydrogen consist mainly of resonant charge exchange with SW protons, and EUV photoionization (Quémerais et al. 2006). The evolution of these effects with solar activity is monitored and the corresponding changes in the H distribution are modeled based on Ly\(\alpha\) back-scattering observations with SOHO/SWAN since 1996 (Koutroumpa et al. 2019). For helium atoms, radiation pressure is negligible, therefore the trajectories are dominated by gravity and form a localized enhancement downstream from the Sun, the He focusing cone. Loss processes for He include EUV photoionization (McMullin et al. 2004) and electron impact (Rucinski & Fehr 1989). Monitoring of the loss processes for He is based on empirical formulas based on CELIAS/SEM data (Bzowski et al. 2013), scaled to McMullin et al. (2004).

For the simulations used in this analysis, we calculated the normalized model \(Q\) with neutral distributions corresponding to the solar activity phase to each exposure in the filtered HS12 sample (omitting high H I column density sightlines). The seasonal variation of the normalized model is compared to the observed residuals after subtracting SWCX and the MW contributions in Figure 4. The results also show a yearly modulation, since the scaled neutral densities are roughly axisymmetric around the interstellar flow axis, and produce parallax effects for different observer positions (Koutroumpa 2012; also see a review from Kuntz 2019).

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