TWO NEARBY SUB-EARTH-SIZED EXOPLANET CANDIDATES IN THE GJ 436 SYSTEM

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ABSTRACT

We report the detection of UCF-1.01, a strong exoplanet candidate with a radius 0.66 ± 0.04 times that of Earth (R\textsubscript{E}). This sub-Earth-sized planet transits the nearby M-dwarf star GJ 436 with a period of 1.365862 ± 8 × 10\textsuperscript{-6} days. We also report evidence of a 0.65 ± 0.06 R\textsubscript{E} exoplanet candidate (labeled UCF-1.02) orbiting the same star with an undetermined period. Using the Spitzer Space Telescope, we measure the dimming of light as the planets pass in front of their parent star to assess their sizes and orbital parameters. If confirmed today, UCF-1.01 and UCF-1.02 would be designated GJ 436c and GJ 436d, respectively, and would be part of the first multiple-transiting-planet system outside of the Kepler field. Assuming Earth-like densities of 5.515 g cm\textsuperscript{-3}, we predict both candidates to have similar masses (~0.28 Earth-masses, M\textsubscript{E}, 2.6 Mars-masses) and surface gravities of ~0.65 g (where g is the gravity on Earth). UCF-1.01’s equilibrium temperature (T\textsubscript{eq}, where emitted and absorbed radiation balance for an equivalent blackbody) is 860 K, making the planet unlikely to harbor life as on Earth. Its weak gravitational field and close proximity to its host star imply that UCF-1.01 is unlikely to have retained its original atmosphere; however, a transient atmosphere is possible if recent impacts or tidal heating were to supply volatiles to the surface. We also present additional observations of GJ 436b during secondary eclipse. The 3.6 \mu m light curve shows indications of stellar activity, making a reliable secondary eclipse measurement impossible. A second non-detection at 4.5 \mu m supports our previous work in which we find a methane-deficient and carbon monoxide-rich dayside atmosphere.

Key words: planets and satellites: detection – stars: individual (GJ 436) – techniques: photometric

Online-only material: color figures, supplemental data (FITS) file (tar.gz)

1. INTRODUCTION

The search for Earth-sized planets around main-sequence stars has progressed exponentially in the last year. Recent discoveries include two Earth-sized planets (0.868 and 1.03 Earth radii, R\textsubscript{E}) from the Kepler-20 system (Fressin et al. 2012), two planet candidates (0.759 and 0.867 R\textsubscript{E}) from the KIC 05807616 system (Charpinet et al. 2011), and a three-planet system (0.78, 0.73, and 0.57 R\textsubscript{E}) orbiting KOI-961 (Muirhead et al. 2012).

The search for a second planet in the GJ 436 system began shortly after the transit detection and confirmed eccentric orbit of GJ 436b (Gillon et al. 2007; Deming et al. 2007). In 2008, a ~5 M\textsubscript{E} planet on a 5.2 day orbit was proposed by Ribas et al. (2008; later retracted) due to three lines of evidence. First, the lack of detection of GJ 436b transits at the time of its 2004 discovery using radial-velocity (RV) measurements (Butler et al. 2004) suggests a change in orbital inclination due to a perturber. Second, given a circularization timescale of ~30 Myr (Deming et al. 2007) and the estimated 6 Gyr age of the system (Torres 2007), GJ 436b’s non-circular orbit suggests another planet is pumping up its eccentricity. Third, there was evidence of a residual low-amplitude RV signal in a 2:1 mean-motion resonance with GJ 436b (Ribas et al. 2008). The inferred planet was discredited by orbital-dynamic simulations (Bean & Seifahrt 2008; Demory et al. 2009) and the absence of transit timing variations (TTVs) with two transit events with the Near-Infrared Camera and Multi-Object Spectrograph camera on the Hubble Space Telescope (Pont et al. 2009) and over a 254 day span using ground-based H-band observations (Alonso et al. 2008).

Ballard et al. (2010b)’s analysis of 22 days of nearly continuous observations of GJ 436 during NASA’s EPOXI mission ruled out transiting exoplanets >2.0 R\textsubscript{E} outside GJ 436b’s 2.64 day orbit (out to a period of 8.5 days) and >1.5 R\textsubscript{E} interior to GJ 436b, both with a confidence of 95%. Aided by a ~70hr Spitzer observation of GJ 436 at 8.0 \mu m, Ballard et al. (2010a) postulated the presence of a 0.75 R\textsubscript{E} planet with a period of 2.1076 days. However, the predicted transit was not detected in an 18 hr follow-up observation with Spitzer at 4.5 \mu m. The candidate transit signals in the EPOXI data were likely the result of correlated noise (Ballard et al. 2010a).

In this paper we present Spitzer primary-transit observations of UCF-1.01 and UCF-1.02 at 4.5 \mu m (including an independent analysis), a phase curve of GJ 436b at 8.0 \mu m in which transits of UCF-1.01 are modeled, and a publicly available EPOXI light curve phased to the period of UCF-1.01. We also include secondary-eclipse observations of GJ 436b at 3.6 and 4.5 \mu m.

In Section 2, we describe the observations and data analysis. Section 3 presents time-series image denoising (TIDE; a wavelet-based technique used to improve image centers) and provides an example analysis using a fake data set. In Section 4, we discuss the specific steps taken with each of the six Spitzer data sets, the details of our independent analysis, and transit results from the EPOXI light curve. Section 5 describes how
we eliminate false positives, our radial-velocity analysis, mass constraints on both sub-Earth-sized exoplanets, and orbital and atmospheric constraints on UCF-1.01. Finally, we give our conclusions in Section 6 and supply the full set of best-fit parameters with uncertainties in Appendix B.

2. OBSERVATIONS AND DATA ANALYSIS

2.1. Observations

We observed GJ 436 at 3.6 and 4.5 μm using Spitzer’s InfraRed Array Camera (IRAC; Fazio et al. 2004). Including the two previously analyzed data sets listed in Table 1, we present six Spitzer observations spanning just over three years.

2.2. POET Pipeline and Modeling

Our Photometry for Orbits, Eclipses, and Transits (POET) pipeline produces systematics-corrected light curves from Spitzer Basic Calibrated Data. We flag bad pixels, calculate image centers from a Gaussian fit, and apply interpolated aperture photometry (Harrington et al. 2007) with a broad range of aperture sizes in 0.25 pixel increments. To achieve more precise image centers in the 2010 January 28 data set, we utilize TIDe (see Section 3). For a more detailed description of POET, see Campo et al. (2011) and Stevenson et al. (2012).

We model the light curve as follows:

\[ F(x, y, t) = F_0 E(t) R(t) S(t) M(x, y), \]

where \( F(x, y, t) \) is the measured flux centered at position \((x, y)\) on the detector at time \(t\); \( F_0 \) is the (constant) system flux outside of transit events; \( E(t) \) is the primary-transit or secondary-eclipse model component; \( R(t) = 1 - e^{-p(t-r_0)} \) is the time-dependent ramp model component with free parameters \( r_0 - r_3 \); \( S(t) = s_0 \cos[2\pi(t - s_1)/p] \) is the phase variation at 8.0 μm with free parameters \( s_0 \) and \( s_1 \) and \( p \) being the fixed period of GJ 436b; and \( M(x, y) \) is the Bilinearly-Interpolated Subpixel Sensitivity (BLISS) map. We follow the method described by Stevenson et al. (2012) when determining the optimal bin sizes of the BLISS maps.

The uniform-source and small-planet equations (Mandel & Agol 2002) describe the secondary-eclipse and primary-transit model components. We apply a nonlinear stellar limb-darkening model (Claret 2000; Beaulieu et al. 2008) to UCF-1.01 transits with coefficients \( a_1 - a_4 = (0.79660, -1.0250, 0.82228, -0.26800) \). Spitzer data has well documented systematic effects that our Levenberg–Marquardt minimizer fits simultaneously with the transit/eclipse parameters. BLISS mapping (Stevenson et al. 2012) models the position-dependent systematics (such as intrapixel variability and pixelation) and linear or asymptotically constant exponential functions model the time-dependent systematics.

A Metropolis random-walk Markov-chain Monte Carlo (MCMC) algorithm assesses the uncertainties (Campo et al. 2011). Each MCMC run begins with a least-squares minimization, a rescaling of the Spitzer-supplied uncertainties so that the reduced \( \chi^2 \) = 1, and a second least-squares minimization using the new uncertainties. We test for convergence every 10^5 steps, terminating only when the Gelman & Rubin (1992) diagnostic for all free parameters has dropped to within 1% of unity using all four quarters of the chain. We also examine trace and autocorrelation plots of each parameter to confirm convergence visually. We estimate the effective sample size (ESS; Kass et al. 1998) and autocorrelation time for each free parameter and apply the longest autocorrelation time from each event to determine the number of steps between independent samples in each MCMC chain. We place a prior on UCF-1.01’s semimajor axis \( (a/R_\ast) = 9.1027^{+0.0067}_{-0.0067} \) by applying its known period and GJ 436b’s well constrained semimajor axis and period (Knutson et al. 2011) to Kepler’s third law. Without a prior, the uncertainties for the semimajor axis (and any correlated parameters) are larger, but not unstable. We also place a flat prior on UCF-1.02’s ingress/egress time of \(<0.1 \text{ hr} \) because it is unconstrained by the data.

3. TIME-SERIES IMAGE DENOISING

Here we describe an application of wavelets that improves image centering, resulting in more precise aperture photometry and better handling of the position-dependent systematics. Readers primarily interested in the science results can skip to Section 4.

3.1. Introduction

Photon noise in short exposures can cause significant shifts between the fitted and real stellar centers. With imprecise centering over multiple frames, varying amounts of light fall within the improperly placed apertures, thus increasing light-curve scatter. The sensitivity to precise centering increases with smaller aperture sizes, causing a given change in aperture position to produce larger changes in flux. To improve centering, one could sum many exposures, but wavelet filtering allows the same noise reduction over a shorter time span. This is important because Stevenson et al. (2010) detect 0.04 pixel (0.05 arcsec) pointing variations for IRAC data over ~5 s at >10σ, which limits the span of an averaging window to a few seconds. Our wavelet filter is called TIDe (pronounced “tidy”). It affects only high-frequency components, such as photon noise, without

Table 1

| Observation Date   | Duration (minutes) | Frame Time (s) | Total Frames | Spitzer Pipeline | Wavelength (μm) | Previous Publications |
|--------------------|--------------------|----------------|--------------|-----------------|-----------------|----------------------|
| 2008 July 14       | 4207               | 0.4            | 588,480      | $18.18.0$       | 8.0             | K10                  |
| 2010 January 28    | 1081               | 0.1            | 488,960      | $18.18.0$       | 4.5             | B10                  |
| 2010 June 29       | 363                | 0.4            | 49,536       | $18.18.0$       | 4.5             | –                    |
| 2011 January 24    | 369                | 0.4            | 51,712       | $18.18.0$       | 4.5             | –                    |
| 2011 February 1    | 369                | 0.1            | 168,576      | $18.18.0$       | 3.6             | –                    |
| 2011 July 30       | 258                | 0.4            | 36,160       | $18.18.0$       | 4.5             | –                    |

Note. a K10 = parts were published by Knutson et al. (2010); B10 = Ballard et al. (2010a).
affecting low-frequency components like transits or eclipses. It retains the time resolution of the data.

In addition to improving aperture photometry, precise centering (see example in Section 3.3) improves our ability to model and remove position-dependent systematics accurately, for example, by reducing the smallest meaningful bin size for BLISS mapping. TIDe does correlate the data in time, which complicates error analysis and makes it computationally intense because the correlation depends on the signal and thus varies in time. So, we use TIDe-cleaned images only for centering (whose uncertainties do not propagate), and perform photometry on the unfiltered images.

As with a windowed (sliding) Fourier transform (WFT), wavelets decompose a signal into independent contributions at each scale and location (similar to frequency and time) within the signal. As an example, the Fourier transform of a piece of music can discern the average pitch and timbre of all the instruments, but wavelets can identify individual notes and the instruments that played them at any given time. The wavelet transform of a univariate time series thus has two dimensions, for location and scale. Unlike the WFT, wavelets do not suffer from a fixed resolution (or window size), so they retain both good temporal resolution for high-frequency events and good scale resolution for low-frequency events. Torrence & Compo (1998) provide an accessible introduction to wavelets.

TIDe’s improvement in precision and benefits to the light-curve fit can vary based on the source brightness, aperture size, BLISS map resolution, etc. This method is applicable to most photon-noise-limited photometric observations where the cadence is significantly shorter than the duration or period of the time-varying object of interest.

3.2. Description of TIDe

TIDe applies discrete wavelet denoising independently to multiple time series, each comprised of the values measured in a single pixel as a function of time (i.e., frame number). Every pixel is associated with such a time series, and each one is denoised independently of adjacent image pixels. The transformed data (known as wavelet coefficients) for each pixel time series have a location (or time) dimension and a scale (or level) dimension. The wavelet coefficients map the discrete wavelet to the data at each scale and instant in time. The lowest level (or finest scale) of decomposition describes how the data change on the shortest timescales. Assuming that this level is dominated by noise, we can eliminate wavelet coefficients with magnitudes below a certain threshold (hard thresholding) or merely attenuate them (soft thresholding) to reduce their contribution to the overall signal. Adjusting a collection of estimates together in this way can be shown to improve the average quality of the estimates by introducing a small bias that is more than compensated for by reduced variance. These techniques can also be applied to successively higher levels, but they have less impact at longer timescales where the signal dominates over the noise. After thresholding, we recombine all of the adjusted wavelets to generate a less-noisy version of the original pixel time series. For each frame, an image is re-created from the many denoised time series, and centering is performed using that image. There is no explicit spatial denoising, but to the extent that there are spatial correlations between images at different epochs, there is an implicit spatial denoising in the processed image that improves center estimation. The effectiveness of TIDe is determined by the threshold at which wavelet coefficients are zeroed, the type of thresholding technique applied, and the number of levels to which the method is applied (Donoho & Johnstone 1994; Chang et al. 2000).

Various wavelet thresholding techniques exist, each with its own advantages and disadvantages. Two common methods for suppressing noise are hard and soft universal thresholding and are defined, respectively, as follows:

$$\omega = y I(|y| > T),$$  \hspace{1cm} (2)

$$\omega = \text{sgn}(y)(|y| - T) I(|y| > T),$$  \hspace{1cm} (3)

where \(y(\omega)\) are the original (denoised) wavelet coefficients at a particular level, \(I\) is the Indicator function (1 if true, 0 if false), and \(T\) is some threshold limit. In both instances, if a particular wavelet coefficient, \(y_i\), is less than \(T\), then \(\omega_i = 0\). With hard thresholding, the remaining coefficients are unaltered; however, soft thresholding shrinks these coefficients by the threshold limit.

There are many ways to estimate the value of \(T\), including VisuShrink, SURE Shrink, and Bayes Shrink (Chang et al. 2000). With TIDe, we implement the last technique because it establishes a thresholding rule that is optimal in terms of minimizing the expected rms error in the denoised time series under flexible assumptions for the true time-series signal (i.e., it minimizes the Bayes Risk for a squared-error loss function). Bayes Shrink employs soft thresholding because its optimal estimator yields a smaller risk than hard-thresholding’s estimator. The optimal threshold value is determined as follows (see Chang et al. 2000). In some instances, the noise variance, \(\sigma^2\), may be known a priori. If this is not the case, it is estimated from the robust median estimator (Donoho & Johnstone 1994):

$$\sigma = \frac{\text{Median}(Y_j(y))}{0.6745},$$  \hspace{1cm} (4)

where \(Y_j(y)\) represents the wavelet coefficients, \(y\), at the lowest level (or finest scale) of decomposition. Next, we estimate the variance of \(Y(y)\) at a particular level \(j\), assuming zero mean, by

$$\sigma_j^2 = \frac{1}{n} \sum_{i=1}^{n} Y_j^2(y_i),$$  \hspace{1cm} (5)

where \(n\) is the number of wavelet coefficients at that level. Our observation model (data = signal + noise) tells us that \(\sigma_j^2 = \sigma_x^2 + \sigma^2\), where \(\sigma_x^2\) is the signal variance. To account for the case where \(\sigma^2 > \sigma_x^2\), we calculate \(\sigma_x^2\) as follows:

$$\sigma_x = \sqrt{\max(\sigma_x^2 - \sigma^2, 0)}.$$  \hspace{1cm} (6)

Finally, the optimal threshold at a particular level is determined by

$$T_j = \frac{\sigma^2}{\sigma_x^2}.$$  \hspace{1cm} (7)

In the event that \(\sigma^2 > \sigma_x^2\) (\(T_j = \infty\)), all of the wavelet coefficients are set to zero.

In this paper, we use the Biorthogonal 5.5 discrete wavelet from the PyWavelets package to apply soft thresholding with Bayes Shrink to the designated scale levels.
3.3. TIDe Example

We generated a series of 1,000 test frames, each containing a 2D Gaussian with a width of 0.7 pixels, a peak flux of 1000, and centered at (4.5, 4.5) in a 10 × 10 frame with the lower-left corner indexed as (0, 0). We then added a background flux offset of 100 and applied Poisson noise to each frame. We performed 2D Gaussian centering to derive the blue points plotted in Figure 1. For the points in red, we applied TIDe to the frames using a Biorthogonal 5.5 discrete wavelet (from the PyWavelets package) then recalculated the image centers with the same 2D Gaussian centering routine. In each case, only the \( y \) component of the position is plotted for each frame. Using TIDe, the standard deviation in the pointing about the true center decreased from 0.019 to 0.011 pixels, for a typical improvement of \( \sim 40\% \). We see even better results with the 2010 January 28 data set, where TIDe improved the pointing precision by \( \sim 70\% \).

4. LIGHT-CURVE FITS AND RESULTS

We present the scaling of the rms model residuals versus bin size (a test of correlation in time) in Figure 2 for all four 4.5 \( \mu \)m Spitzer observations. Figure 3 displays our reanalysis of GJ 436 data (Ballard et al. 2010a) plus three new Spitzer light curves at 4.5 \( \mu \)m. Two fortuitous detections of UCF-1.01 appeared during atmospheric characterization observations of GJ 436b (Stevenson et al. 2010). Using these data and a tentative detection at 8.0 \( \mu \)m (see Section 4.6) to estimate its orbital period, we extrapolated UCF-1.01 transit times forward by six months to predict an event (2011 July 30) during the next observing window. We supply correlation plots and histograms.
in Appendix A and the full set of best-fit parameters from a $2.4 \times 10^6$-iteration joint fit in Appendix B. Below, we discuss each observation in detail to explain how we arrived at the final results.

### 4.1. 2010 January 28 (4.5 $\mu$m Spitzer Observation)

*Spitzer* program 541 (Sarah Ballard, PI) monitored GJ 436 continuously for $\sim$18 hr using 0.1 s exposures. The short exposure time allows us to apply TIDe to the lowest four levels (L4) of wavelet decomposition (see Section 3), resulting in a maximum affected time resolution of 1.6 s. In Stevenson et al. (2010), we detect *Spitzer* pointing changes on timescales as short as $\sim$5 s, longer than TIDe’s timescale. In calculating image centers with and without TIDe, we find that the position consistency between consecutive denoised frames improves by more than a factor of three, resulting in an rms of 0.0015 pixels in $x$ and 0.0011 pixels in $y$. More precise image centers decrease flux scatter with smaller aperture sizes and aid the BLISS map in modeling the position-dependent systematics. We apply $5 \times$-interpolated aperture photometry to the unmodified frames to avoid the computationally prohibitive calculation of estimating uncertainties for the denoised frames, which are correlated in time.

Photometry generates consistent transit depths for all tested apertures from 1.25 to 4.50 pixels, but an aperture size of 2.25 pixels produces the lowest standard deviation of the normalized residuals (SDNR). We estimate the background flux using an annulus from 7 to 15 pixels centered on the star. The light curve (see Figure 4) exhibits a strong initial increase in pixel sensitivity that we do not model (preclip, $q = 10,000$). As with Ballard et al. (2010a), we detect excess flux (possibly due to stellar activity) near BJD 2455225.23 that contributes to the observed correlated noise in Figure 2. We note that frames 19,780–19,839, 82,180–82,239, 165,380–165,439, 419,780–419,839, and 451,780–451,839 are shifted horizontally by one pixel, so we flag these frames as bad. A probable micrometeor impact at BJD $\sim$2,455,224.976 caused a sudden shift in pointing before returning to its original location. Simultaneously, the background scatter increased by $\sim$50% and remained elevated until the end of the observation. We apply a BLISS map bin size ($x, y$) of 0.007 $\times$ 0.005 pixels and set the minimum number of points per bin to six to disregard the observed excursion.

### 4.2. 2010 June 29 (4.5 $\mu$m Spitzer Observation)

Our *Spitzer* program 60003 (Joseph Harrington, PI) monitored GJ 436 for six hours using 0.4 s exposures. The mean image center is located at pixel (15, 25), near the top of the $32 \times 32$ array, thus restricting aperture sizes to $\leq 5.50$ pixels. Using a background sky annulus from 10 to 30 pixels, we find that the lowest SDNR occurs with a $5 \times$-interpolated aperture 5.00 pixels in radius. The BLISS map uses bins of size $0.006 \times 0.006$ pixels and with at least four points per bin. We test image centers generated from L3 TIDe (3.2 s maximum time resolution) but find no improvement in the SDNR. This is likely due to the smaller improvement in image centers and significantly larger aperture size, relative to the 2010 January 28 data set. The final analysis did not use TIDe. For this data set, the telescope pointing does not stabilize until midway through the transit of UCF-1.02 (see Figure 5). As a result, the position-dependent systematic is poorly constrained during and prior to the transit. This may be the source of UCF-1.02’s variable transit duration, which decreases with smaller aperture sizes. More observations are necessary to confirm its parameters.
4.3. 2011 January 24 (4.5 μm Spitzer Observation)

Spitzer program 60003 performed a second six-hour observation of GJ 436 with 0.4 s exposures. We find that 10x-interpolated aperture photometry outperforms 5x-interpolated and minimizes SDNR with an aperture size of 5.25 pixels and a background sky annulus from 10 to 30 pixels. We flag 54 frames (28,426–28,479) as bad due to a one-pixel horizontal shift, as observed previously in a data set above. We clip the first 6000 observations due to a strong increase in flux, possibly due to stellar activity (see Figure 3). Near 2455585.771, we observe a sudden shift in the telescope pointing that, again, correlates with an increase in background noise. To remove this excursion from our models, the BLISS map uses bins with eight or more points and a size of 0.016 × 0.008 pixels. As with the previous data set and for the same reasons, TIDe centers have little effect on the resulting photometric light curve.

4.4. 2011 February 1 (3.6 μm Spitzer Observation)

Our Spitzer program 60003 also observed GJ 436 at 3.6 μm with 0.1 s exposures. We apply 5x-interpolated aperture photometry with an aperture size of 2.75 pixels and a background sky annulus from 7 to 15 pixels. We clip the first 10,000 frames due to a steep ramp and frames 70,000–125,000 due to suspected stellar activity (see Figure 6). Because GJ 436b’s time of secondary eclipse occurs during the period of increased stellar activity, we do not fit the eclipse or calculate uncertainties.

4.5. 2011 July 30 (4.5 μm Spitzer Observation)

Spitzer monitored GJ 436 for 4.3 hr using 0.4 s exposures (program 70084, Joseph Harrington, PI). Photometry generates consistent transit depths for apertures between 1.75 and 6.00 pixels. The final run applies 10x-interpolated, 5.00 pixel aperture photometry with a background sky annulus from 10 to 30 pixels. During these observations, the telescope pointing experiences two deviations, at BJD 2,455,772.766 and 2,455,772.870. The background variance increases with the first event but slightly decreases with the second event. BLISS mapping utilizes a bin size of 0.012 × 0.006 pixels with a minimum of six points per bin to exclude points from either excursion. Again, TIDe centers have little effect on the resulting photometric light curve.

4.6. 2008 July 14 (8.0 μm Spitzer Observation)

Spitzer program 50056 (Heather Knutson, PI) observed GJ 436 for ∼70 hr from 2008 July 12 to 2008 July 15. At the best aperture size of 3.75 pixels (and a background sky annulus from 7 to 15 pixels), we find that the light curve exhibits a measurable position-dependent systematic, identified as pixelation (Stevenson et al. 2012). The BLISS map fits and removes pixelation (see Figure 7) using a bin size of 0.022 × 0.022 pixels and at least four points per bin. We model the initial time-dependent ramp using an asymptotically constant exponential function after clipping the first 3000 frames. A sinusoidal function with a linear correction fits the phase variation of GJ 436b (see Figure 8). We set a prior on the inclination and semimajor axis of UCF-1.01 using the best-fit results from the 4.5 μm joint fit. The UCF-1.01 transit at BJD 2,454,662.328 is the same candidate transit reported by Ballard et al. (2010a) using a ∼2.1 day period estimated from EPOXI observations. Their Figure 5 incorrectly reports the BJD. We used the timing of this transit to successfully predict the 2001 July 30 transit. The best-fit radius ratio from both transit events in this light curve is 0.010 ± 0.003.
which is consistent with the best-fit result using the four 4.5 \(\mu m\) light curves.

### 4.7. Independent Analysis

We sought an independent analysis to confirm our results. Nikole Lewis analyzed each of the 4.5 \(\mu m\) data sets without knowing the times or depths of the transits. In addition to using her own photometric pipeline, she applied a new pixel-mapping routine that shares a heritage with the method from Ballard et al. (2010a). This new pixel-mapping method was developed to recover the relative flux variations as a function of orbital phase from the Spitzer 3.6 \(\mu m\) and 4.5 \(\mu m\) full orbit light curves of HD 189733b, HD 209458b, HAT-P-2b, and HAT-P-7b (PI: Knutson; program 60021). Similar to the BLISS method, the pixel-mapping technique developed by Lewis uses nearest neighbors to calculate flux as a function of position on the detector, but in her method the distances are weighted according to a Gaussian distribution. In addition to stellar centroid positions, Lewis makes use of the “noise pixel” parameter given in frame headers to determine the nearest-neighbors to a given data point (Knutson et al. 2012). This routine improves on Ballard’s method by calculating the pixel map at each iteration without being computationally prohibitive.

Pixel mapping is essential to detecting the weak transit signals in these data. For example, the 2010 January 28 data set requires an accurate pixel mapping routine, at minimum, to detect UCF-1.01 and benefits from more precise image centers with TIDe to more clearly distinguish UCF-1.02. We have found that without a pixel-mapping routine, one cannot reproduce all of the observed transits. Lewis uncovered transits of UCF-1.01 in the 2010 June 29, 2011 January 24, and 2011 July 30 data sets with ease and, once informed of the additional planet, identified individually, Lewis performed a simultaneous fit between all four data sets using a Levenberg–Marquardt minimization scheme. An MCMC algorithm determined the uncertainty in the fit parameters as well as identified other possible solutions. The goal of this analysis was to confirm the presence and shape of transit(s) in each data set. Improvements to treatment of the systematics in these observations is possible, but they are unlikely to significantly change the estimated planetary parameters.

### 4.8. EPOXI Observation

NASA’s EPOXI mission observed GJ 436 nearly continuously during 2008 May 5–29 (Ballard et al. 2010b). The light-curve data are available from EPOXI’s archive. After masking the transits of GJ 436b, we divide the light curve by the median flux value, phase it according to the best-fit UCF-1.01 period (see Table 2), and bin the results. Figure 9 illustrates a visible decrease in the observed flux at the correct phase that is consistent with the transit depth and duration of UCF-1.01 derived from the Spitzer data. The quality of the light curve is such that the data neither prove nor disprove the existence of UCF-1.01.

### 5. DISCUSSION

Without continuous monitoring of GJ 436 for two consecutive transits at the most photometrically precise wavelengths (3.6 and 4.5 \(\mu m\)), we isolate the true period from integer multiples or whole number fractions by other means. Integer multiples (i.e., 2, 3, 4 . . .) of the orbital period (see Table 2) cannot account for all of the observed transits; whole number fractions (i.e., 1/2, 1/3, 1/4 . . .) are eliminated by investigating the bevy of available GJ 436 Spitzer data at predicted transit times. We find evidence against periods of ∼0.6829 and
Table 2  
Transit Model Best-fit Values and Other Parameters

| Parameters                      | UCF-1.01  | UCF-1.02  |
|---------------------------------|-----------|-----------|
| $R_p/R_\oplus$                  | 0.0138±0.0009$^a$ | 0.0136±0.0012 |
| $i$ (°)                         | 85.17±0.16  | –         |
| $a/R_\ast$                      | 9.10±0.07$^a$ | –         |
| Impact parameter                | 0.77±0.15  | –         |
| Transit depth (ppm)             | 190±25     | 186±30$^a$ |
| Duration ($t_{\text{d}}$, hr)   | 0.76±0.15  | 1.04±0.26$^a$ |
| Ingress/egress (hr)             | 0.025±0.002 | <0.1$^a$ |
| Transit times (MJD$^b$)         | 5225.090±0.004 | 5225.026±0.003$^a$ |
| Ephemeris (MJD$^b$)             | 5376.7078±0.0024 | 5376.5685±0.003$^a$ |
| Radius ($R_\oplus$)            | 0.06±0.04  | 0.65±0.06  |
| Mass ($M_\oplus$)$^c$          | 0.28±0.06  | 0.27±0.07  |

Notes.  
$^a$ Fitted values.  
$^b$ MJD = BJD−2,450,000.  
$^c$ We choose the median value because the distribution is bimodal.  
$^d$ Assuming an Earth-like density of 5.515 g cm$^{-3}$.  

Figure 10.  
EPOXI light curve phased to the period of UCF-1.01 using the best-fit period and nearest ephemeris time (2008 July 14 data set). Blue circles represent the binned EPOXI data with 1σ uncertainties. The red cross depicts the binned EPOXI data with 1σ uncertainties. The red circle represents the position of the GJ 436 system for this observation and at each transit epoch of UCF-1.01. Red circles indicate the minimum photometric aperture size (1.25 pixels) for which transit signals from the first and last confirmed events may still be clearly distinguished against the background noise. If a background system were the source of the transit-like events, it must put light in the overlapping region. To produce the observed transit depth, the hypothetical system must be no more than 9.3 mag fainter than GJ 436, assuming a total eclipse of one of the objects. We eliminate objects brighter than $\Delta H = 12.7$ relative to GJ 436 with a confidence of 5σ. There are also no objects listed in any catalog within this region.

Figure 11.  
Very Large Telescope $H$-band observation on 2007 March 20 using the NAOS-CONICA instrument with adaptive optics (Montagnier et al. 2012). We search for faint background systems by blocking the light from GJ 436 using a 0.7 Lyot coronagraphic mask. The dark green lines are mask support wires. The “+” symbols indicate the position of the GJ 436 system for this observation and at each transit epoch of UCF-1.01. Red circles indicate the minimum photometric aperture size (1.25 pixels) for which transit signals from the first and last confirmed events may still be clearly distinguished against the background noise. If a background system were the source of the transit-like events, it must put light in the overlapping region. To produce the observed transit depth, the hypothetical system must be no more than 9.3 mag fainter than GJ 436, assuming a total eclipse of one of the objects. We eliminate objects brighter than $\Delta H = 12.7$ relative to GJ 436 with a confidence of 5σ. There are also no objects listed in any catalog within this region.

5.2. Instability Hypothesis

In this section we consider an alternate hypothesis to that of detecting two sub-Earth-sized exoplanets, that the observed variations are the result of instrumental or stellar instabilities. We begin by calculating the probability of observing UCF-1.01 and UCF-1.02 by chance. Then, we quantify the occurrence rate of transit-like instabilities and estimate the probability that these instabilities are periodic. Finally, we compare our model fits to the null hypothesis, which is expressed by a model that does not contain planet parameters, to see if the additional free parameters are justified.

In search of transit signals in the GJ 436 system, we examined 11 light curves at 3.6 and 4.5 $\mu$m (not counting the 2011 July 30 data set in which we predicted the transit). Both channels have the photometric stability necessary to detect GJ 436c. Of the 71.3 hr of data, there are eight transit or eclipse events of GJ 436b, each lasting $\sim$1 hr in duration. Since we cannot distinguish overlapping transits, we have 63.3 hr of usable data with an average light-curve duration of $\sim$5.75 hr. Given that the period of UCF-1.01 is 1.3659 days, the probability that a transit will occur in a typical event is 17.5%. Using the binomial
distribution, we calculate a 30.1% chance of observing three or more transits of UCF-1.01 in the 11 available light curves. Recall that our fourth transit event of UCF-1.01 was predicted, rather than occurring by chance, so it does not enter into the calculation.

We repeat the above calculation for UCF-1.02 but must first estimate its orbital period by considering the transit duration ratio between itself and GJ 436b. We find that the durations are nearly identical; however, both planets are unlikely to occupy the same orbit. So, we perform two sets of calculations: one for each side of the 1-sigma uncertainty in UCF-1.02’s transit duration. Using a period of 5.563 days, the probability of observing two or more UCF-1.02 transits is 7.9%. Using a period of 1.785 days, the probability of observing two or more transits increases to 44.6%. The combined probability of observing both planets ranges from 2.3% to 13.4%.

We compare these results to the alternate hypothesis, namely that the observed variations are the result of instrumental or stellar instabilities. To begin, we analyzed nearly 120 hr of GJ 1214 data at 4.5 μm (Spitzer program 70049). This M dwarf is similar to GJ 436 and should exhibit similar levels of activity (stellar instabilities). If the instabilities are instrumental, then it should not matter which star we analyze unless the instabilities are flux-dependent (GJ 436 is almost 3 mag brighter than GJ 1214 in the infrared). From our GJ 1214 light-curve results, we identify two transit-like events based on their depths (> 200 ppm) and durations (~1 hr). Assuming these events are not the result of planet transits, for any given hour of 4.5 μm observations, there is a 1.7% probability of having an instability event. We then apply the binomial distribution to determine that the probability of detecting five or more instabilities in 63.3 hr of data is 0.42%. Recall that we do not count the 2011 July 30 data set or use times during GJ 436b transits/eclipses. If we assume that the instabilities only appear at 4.5 μm, the probability of detecting five or more instabilities in 44.7 hr of data decreases to 0.088%.

Since we cannot find a physical mechanism for reducing the stellar flux in a transit-like way with a repeatable period, any observed instabilities must be random events. We consider the probability of detecting four random instability events that happen to coincide with a given period (in this case, 1.3659 days). The first two instability events establish the “period” under consideration. As calculated above, the third and fourth instability events each have a 1.7% probability of occurring within 30 minutes of the established period (total time window is 1 hr). Their combined probability is 0.029%.

We conclude that the single-planet hypothesis is 72 times more likely than the most favorable instrumental/stellar-instability scenario and 1040 times more likely than detecting four random instability events that happen to coincide with a given period. The two-planet hypothesis is 5.5–32 times more likely than the most favorable instrumental/stellar-instability scenario and 79–460 times more likely than detecting four random instability events that happen to coincide with a given period.

Finally, we test the strength of our two sub-Earth-sized exoplanet candidates by comparing various fits to the null
hypothesis, which asserts that there are no new planets. Recall that a lower \( \Delta \text{BIC} \) value indicates that the additional free parameters are warranted in the model fit. Relative to the null hypothesis, \( \Delta \text{BIC} \) decreases by 11.4 when we include UCF-1.01’s transit parameters in a joint model fit. Alternatively, if we add only UCF-1.02’s transit parameters then \( \Delta \text{BIC} \) increases by 36.2. Including both planets’ transit parameters in a joint model fit results in an increase in \( \Delta \text{BIC} \) of 14.5, relative to the null hypothesis. Thus, the BIC favors a model that includes UCF-1.01 but disfavors models that include UCF-1.02. This result is directly related to the number of observed transits for each planet candidate and indicates that we need to obtain more than two transit observations of UCF-1.02 to increase the detection significance and surpass the BIC’s penalty for additional free parameters. We conclude that the available data support UCF-1.01 as a strong exoplanet candidate and signify that UCF-1.02 is a weak exoplanet candidate.

5.3. Radial-velocity Constraints

The 3.6 m ESO telescope at La Silla Observatory (Mayor et al. 2003; Pepe et al. 2004) utilized the HARPS spectrograph with the settings described by Bonfils et al. (2011) to obtain 171 observations of GJ 436 at 550 nm. Xavier Bonfils (private communication) provided us with the extracted, unpublished RV measurements so that we could attempt to constrain the mass of UCF-1.01. We retained 159 data points (12 were removed due to the Rossiter–McLaughlin effect). To these data, we added 41 GJ 436b primary transit times (Knutson et al. 2011 and references therein), 14 GJ 436b secondary eclipse times (Stevenson et al. 2010; Knutson et al. 2011), and an 8.0 \( \mu \)m photometric light curve from Deming et al. (2007). The light curve (retrieved from the Infrared Processing and Analysis Center, IPAC) is binned into 445 points and normalized to remove the time-dependent ramp.

We apply a two-planet model with the transit ephemeris for the second planet fixed to the best-fit value listed in Table 2 and the eccentricity fixed to zero. The fit utilizes the empirical stellar density calibration of Enoch et al. (2010) to determine the stellar mass, in addition to other system parameters, granting this fit a much broader scope than the modeling described by Campo et al. (2011). We employ a Levenberg–Marquardt minimizer to find the best-fit parameters to our model and an MCMC routine with 106 iterations to estimate uncertainties. We express our \( \chi^2 \) function as follows:

\[
\chi^2 = \sum_i \left[ \frac{v_i - \bar{v}_i}{\sigma_{v,i}} \right]^2 + \sum_j \left[ \frac{t_j - \bar{t}_j}{\sigma_{t,j}} \right]^2 + \sum_k \left[ \frac{o_k - \bar{o}_k}{\sigma_{o,k}} \right]^2 + \sum_m \left[ \frac{p_m - \bar{p}_m}{\sigma_{p,m}} \right]^2,
\]

where \( v, t, o, \) and \( p \) represent the HARPS radial velocities, primary-transit times, secondary-eclipse times, and photometric data, respectively. The overlined quantities indicate computed values and \( \sigma \) represents the uncertainty for each measurement. We adjust for transit-eclipse light travel times and for leap seconds in this fit. Using the above data with an estimated stellar jitter of 1.7 m s\(^{-1}\), we do not detect the signal of the second planet but cannot repudiate its existence. The 3\( \sigma \) upper limit of the semi-amplitude is 0.6 m s\(^{-1}\), corresponding to an upper limit of 0.6 \( M_{\oplus} \), which is larger than our mass constraints using the density arguments below.

5.4. Mass Constraints

Unable to effectively constrain the mass of UCF-1.01 using RV data, we consider a range of possible bulk densities for a terrestrial-sized planet (see Figure 13). Given a mean bulk density between 3 and 8 g cm\(^{-3}\), we limit the mass of UCF-1.01 to be 0.15–0.40 \( M_{\oplus} \) and estimate the surface gravity to be 0.36–0.94 g. We place similar limits on the mass and surface gravity of UCF-1.02. Assuming an Earth-like density of 5.515 g cm\(^{-3}\), we estimate masses of 0.28 and 0.27 \( M_{\oplus} \) for UCF-1.01 and UCF-1.02, respectively, which correspond to surface gravities of \( \sim \)0.65 times that on Earth.

5.5. Orbital Constraints

UCF-1.01 may exhibit TTVs due to gravitational interactions with GJ 436b in a near-2:1 orbital resonance or with UCF-1.02, which has an unknown orbit. This may explain why UCF-1.01’s transit time is 20 minutes early in the 2010 January 28 data set; however, the parameter’s probability distribution is bimodal (see Figure 14) and the other peak is only 6 ± 7 minutes early. The three remaining UCF-1.01 transit times occur within five minutes of their predicted times and have a typical uncertainty of \( \pm 3 \) minutes. More precise observations could establish whether these deviations are TTVs.

Using the known orbital parameters of GJ 436b and UCF-1.01, we performed orbital-stability simulations using the Mercury numerical integrator (Chambers 1999). Assuming an Earth-like density of 5.5 g cm\(^{-3}\), the predicted mass of UCF-1.01 is 0.28 \( M_{\oplus} \). We supplied the code with initial starting conditions, listed in Table 3, based on transit times from the 2011 January 24 data set. Our results indicate that the orbits are stable out to at least 100 Myr. The best-fit line shows a change in semimajor axis of 5.3e-06 AU Gyr\(^{-1}\). The osculating UCF-1.01 orbital parameters exhibit a periodic trend every \( \sim \)35 years wherein the eccentricity varies between 0 and 0.21, the peak-to-trough inclination amplitude is 3:2, and TTVs vary from \( \pm 200 \) to \( \pm 3 \) minutes. A \( \sim \)40 day periodic trend is also evident but with smaller variations in the osculating orbital parameters. Due to UCF-1.01’s relatively small mass, variations in GJ 436b’s orbital parameters over the 35-year time span are below Spitzer’s sensitivity limits. Next-generation facilities may be able to constrain UCF-1.01’s orbital parameters through improved RV measurements or by measuring its time of secondary eclipse.

5.6. Atmospheric Constraints

UCF-1.01 is unlikely to have retained any original atmosphere due to its weak gravitational field, close proximity to its host star,
and estimated 6 Gyr age of the system (Torres 2007). The planet receives a substantial soft X-ray and extreme-ultraviolet (XUV) flux; we estimate 700–900 erg cm$^{-2}$ s$^{-1}$ (Sanz-Forcada et al. 2011; Ehrenreich et al. 2011), or $\sim$1,000 times the present XUV flux received by the Earth. Such an intense XUV flux leads to a very hot thermosphere and subsequent hydrodynamic escape (Tian 2009). Shortly after formation, outgassing from an Earth-like, silicate-rich mantle could have produced an initial water-vapor-rich atmosphere for UCF-1.01 (Schaefer et al. 2011). However, the water vapor would quickly be photolyzed by ultraviolet radiation at high altitudes, leading to a hydrogen-dominated thermosphere that likely extended to the planet’s Roche distance of $\sim$25,000 km (Erkaev et al. 2007), given the planet’s low gravity. In this situation, the mass-loss rate for energy-limited hydrodynamic flow (Erkaev et al. 2007) implies a hydrogen loss rate of about $8 \times 10^{10}$ g s$^{-1}$ (assuming an XUV heating efficiency of 1), or 1.4 times the planet’s mass lost in 1 Gyr. This indicates that hydrogen was lost from UCF-1.01’s atmosphere very early in its history. Some heavy elements would have been entrained in the hydrodynamic flow, but the early atmosphere would have become increasingly oxidized as hydrogen was lost. Carbon dioxide could then have dominated at some later point in the atmosphere’s history, but even a CO$_2$-rich atmosphere would be unstable. Scaling from hydrodynamic models (Tian 2009), we estimate that carbon would be lost from a CO$_2$-rich atmosphere at $\sim$1 $\times$ 10$^8$ g s$^{-1}$, or 1% of the planet’s mass over its lifetime—an amount likely greater than the planet’s initial inventory of CO$_2$. Atmospheres dominated by molecular nitrogen or oxygen would be lost on even shorter timescales (Tian 2009).

UCF-1.01 could support a transient, present-day atmosphere if recent impacts were to deliver volatiles rather than preferentially erode any atmosphere, or if tidal heating were to supply volatiles from the crust/mantle. The latter scenario is particularly attractive if a recycling mechanism exists for any heavy atmospheric constituents (e.g., volcanic emission of sulfur dioxide, followed by photolysis to sulfur and oxygen atoms, dayside-to-nightside transport, condensation, and subsequent melting and re-vaporization of sulfur deposits). In this speculative scenario, UCF-1.01 could resemble a hot Io that has lost its lighter and more volatile elements. Any transient atmosphere will likely have a low surface pressure and be highly extended, which could fill the Roche lobe and/or produce a tail. Transit observations at ultraviolet wavelengths could confirm or rule out such an extended atmosphere, and one might search particularly at wavelengths in which atomic and ionized sulfur and oxygen would be expected to absorb. Given that volcanically supplied sodium and potassium might be transient atmospheric constituents, visible-wavelength transit observations might also prove useful.

6. CONCLUSIONS

In this paper, we announced the detection of UCF-1.01 and UCF-1.02, two sub-Earth-sized transiting exoplanet candidates orbiting the nearby M dwarf GJ 436. Their detections were made with BLISS mapping and TIDe, the latter of which is a novel wavelet-based technique that decreases high-frequency noise in short-cadence, time-series images to improve image centering precision. We presented four transits of UCF-1.01 and two transits of UCF-1.02 at 4.5 $\mu$m, an independent analysis that confirms our best-fit models results within 1.5$\sigma$, an 8.0 $\mu$m phase curve of GJ 436b that includes transits of UCF-1.01, and EPOXI data that are consistent with the presence of a sub-Earth-sized exoplanet. To definitively establish UCF-1.01 as a planet (to be called GJ 436c), we require only a few hours of additional observations, preferably from another telescope or at least at a different wavelength. Establishing UCF-1.02 as a planet (to be called GJ 436d) would likely require an extended observing campaign to constrain its period then successfully predict a transit. Finally, we confirmed the GJ 436b 4.5 $\mu$m results presented by Stevenson et al. (2010) through an additional non-detection during secondary eclipse; however, we were unable to confirm the strong eclipse depth at 3.6 $\mu$m due to stellar activity. The current data still support a methane-deficient and carbon monoxide-rich dayside atmosphere.

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APPENDIX A
CORRELATION PLOTS AND HISTOGRAMS

We supply the correlation plots and histograms in Figures 14–17 so that others may evaluate our model fits and further examine the asymmetric or bimodal parameter distributions.
Figure 14. Correlation plots and histograms for the 18 hr 2010 January 28 Spitzer observation containing transits of UCF-1.01 and UCF-1.02. We plot every 4000th step in the MCMC chain to decorrelate parameter values. UCF-1.01’s distribution of mid-transit times (midpoints) is bimodal, so we favor the median value over the best-fit value (see Table 2). UCF-1.02’s ingress/egress times are unconstrained from our model fit. (A color version of this figure is available in the online journal.)
Figure 15. Correlation plots and histograms for the 2010 June 29 Spitzer observation containing transits of UCF-1.01 and UCF-1.02. We plot every 4000th step in the MCMC chain to decorrelate parameter values. UCF-1.02’s ingress/egress times are unconstrained from our model fit.

(A color version of this figure is available in the online journal.)
Figure 16. Correlation plots and histograms for the 2011 January 24 Spitzer observation containing a transit of UCF-1.01 and an eclipse of GJ 436b. We plot every 4000th step in the MCMC chain to decorrelate parameter values.

(A color version of this figure is available in the online journal.)
Figure 17. Correlation plots and histograms for the 2011 July 30 Spitzer observation containing a transit of UCF-1.01. We plot every 4000th step in the MCMC chain to decorrelate parameter values.

(A color version of this figure is available in the online journal.)
APPENDIX B

BEST-FIT PARAMETERS

Table 4 displays the best-fit parameter values and uncertainties from our joint light-curve fit. It also contains information to help evaluate the goodness of fit.

| Parameter | 2010 January 28 | 2010 June 29 | 2011 January 24 | 2011 July 30 | 2008 July 14 |
|-----------|-----------------|--------------|-----------------|--------------|--------------|
| Wavelength (µm) | 4.5 | 4.5 | 4.5 | 4.5 | 8.0 |
| Array Position (i, pix) | 14.69 | 14.94 | 14.63 | 14.70 | 14.54 |
| Array Position (j, pix) | 14.92 | 25.31 | 15.20 | 14.98 | 14.52 |
| Position Consistency (δx, pix) | 0.0015 | 0.0025 | 0.0045 | 0.0041 | 0.0055 |
| Position Consistency (δy, pix) | 0.0011 | 0.0039 | 0.0028 | 0.0024 | 0.0052 |
| Aperture Size (pix) | 2.25 | 5.00 | 5.25 | 5.00 | 3.75 |
| Inner Sky Annulus (pix) | 7.0 | 10.0 | 10.0 | 10.0 | 7.0 |
| Outer Sky Annulus (pix) | 15.0 | 30.0 | 30.0 | 30.0 | 15.0 |
| System Flux, F_s (µJy) | 841090 ± 100 | 871540 ± 30 | 819510 ± 30 | 825590 ± 15 | 315195 ± 7 |
| GJ 436 Tr. Midpt.b (MJD_TDB) | – | – | – | – | 4661.50365 ± 0.00012 |
| GJ 436b R_s/R_⋆ | – | – | – | – | 0.0830 ± 0.0006 |
| GJ 436b α/δ | – | – | – | – | 13.0 ± 0.3 |
| GJ 436 Ecl. Midpt.b (MJD_TDB) | – | – | – | – | 4660.417 ± 0.0003 |
| GJ 436 Ecl. Midpt.b (MJD_TDB) | – | – | – | – | 4663.053 ± 0.0003 |
| GJ 436 Ecl. Duration (t_{E-1}, hrs) | – | – | 1.00 | – | 1.02 ± 0.13 |
| GJ 436 Eclipse Depth (ppm) | – | – | 18 ± 28 | – | 500 ± 60 |
| GJ 436 T_0 (K) | – | – | 540 ± 80 | – | 700 ± 30 |
| GJ 436 Amplitude, x0 (ppm) | – | – | – | – | 100 ± 40 |
| GJ 436 Offset, s (MJD_TDB) | – | – | – | – | 4660.39 ± 0.19 |
| UCF-1.01 Midpt.b (MJD_TDB) | 5225.090 ± 0.004 | 5376.7078 ± 0.0021 | 5585.6889 ± 0.0020 | 5772.80699 ± 0.00029 | 4662.328 ± 0.013 |
| UCF-1.01 R_s/R_⋆ | 0.0138 ± 0.0009 | 0.0138 ± 0.0009 | 0.0138 ± 0.0009 | 0.0138 ± 0.0009 | 0.010 ± 0.003 |
| UCF-1.01 cos i | 0.084 ± 0.003 | 0.084 ± 0.003 | 0.084 ± 0.003 | 0.084 ± 0.003 | 0.084 ± 0.003 |
| UCF-1.01 α/δ | 9.10 ± 0.07 | 9.10 ± 0.07 | 9.10 ± 0.07 | 9.10 ± 0.07 | 9.10 ± 0.06 |
| UCF-1.02 Midpt.b (MJD_TDB) | 5225.026 ± 0.003 | 5376.568 ± 0.003 | – | – | – |
| UCF-1.02 Transit Depth (ppm) | 186 ± 30 | 186 ± 30 | – | – | – |
| UCF-1.02 Duration (t_{E-1}, hrs) | 1.05 ± 0.021 | 1.04 ± 0.02 | – | – | – |
| UCF-1.02 Ingress (t_{E-1}, hrs) | 0.06 ± 0.03 | 0.06 ± 0.03 | – | – | – |
| UCF-1.02 Egress (t_{E-3}, hrs) | 0.06 ± 0.03 | 0.06 ± 0.03 | – | – | – |
| Ramp, r_0 | 7.0 ± 2.0 | 0 | 22 ± 12 | 44 ± 11 | 18.1 ± 1.6 |
| Ramp, r_1 | –8.4 ± 0.6 | 0 | 6 ± 8 | 25 ± 8 | –0.6 ± 0.5 |
| Ramp, r_2 | –0.0008 ± 0.0003 | 0.0020 ± 0.0003 | 0 | 0 | –0.00012 ± 0.00006 |
| Ramp, r_3 | 0 | 0.5 | 0 | 0 | 1.5 |
| TIDe | Yes | Yes | No | No | No |
| BLISS Map [M(x, y)] | Yes | Yes | Yes | Yes | Yes |
| Effective Sample Size (ESS) | 341 | 702 | 398 | 675 | 415 |
| Minimum # of Points Per Bin | 6 | 4 | 8 | 6 | 4 |
| Total Frames | 488960 | 49536 | 51712 | 36160 | 588480 |
| Rejected Frames (%) | 0.178 | 0.527 | 0.673 | 0.465 | 0.393 |
| Frames Used | 477106 | 48777 | 44728 | 35172 | 583049 |
| Free Parameters | 6 | 10 | 5 | 4 | 18 |
| AIC Value | 605808 | 605808 | 605807 | 605808 | 583067 |
| BIC Value | 606091 | 606091 | 606090 | 606091 | 583270 |
| SDNR | 0.00535600 | 0.00253643 | 0.00257029 | 0.00258144 | 0.00508140 |
| Uncertainty Scaling Factor | 0.31734 | 0.17676 | 1.06515 | 0.98102 | 1.04102 |
| Photon-Limited S/N (%) | 84.3 | 82.2 | 84.0 | 83.2 | 84.3 |

Notes.

a rms frame-to-frame position difference.

b MJD = BJD−2,450,000.

c We exclude frames during instrument/telescope settling, for insufficient points at a given knot, and for bad pixels in the photometry aperture.
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