Lubricity of gold nanocrystals on graphene measured using quartz crystal microbalance

M. S. Lodge, C. Tang, B. T. Blue, W. A. Hubbard, A. Martini, B. D. Dawson & M. Ishigami

In order to test recently predicted ballistic nanofriction (ultra-low drag and enhanced lubricity) of gold nanocrystals on graphite at high surface speeds, we use the quartz microbalance technique to measure the impact of deposition of gold nanocrystals on graphene. We analyze our measurements of changes in frequency and dissipation induced by nanocrystals using a framework developed for friction of adatoms on various surfaces. We find the lubricity of gold nanocrystals on graphene to be even higher than that predicted for the ballistic nanofriction, confirming the enhanced lubricity predicted at high surface speeds. Our complementary molecular dynamics simulations indicate that such high lubricity is due to the interaction strength between gold nanocrystals and graphene being lower than previously assumed for gold nanocrystals and graphite.

A simple phenomenological formula, \( F = \mu N \), where \( \mu \) is the coefficient of friction and \( N \) is the normal force, governs macroscopic friction. Nanoscale contacts between surface asperities are assumed to determine \( \mu \), but the fundamental science of friction at nanoscale, nanotribology, is still in its infancy and many unsolved problems remain.

One of the most promising discoveries in nanotribology is structural lubricity\(^1\): low friction between atomically incommensurate surfaces. Structural lubricity was first anticipated in theoretical considerations of weakly-coupled incommensurate structures\(^2,3\) and has been observed on various surfaces such as mica\(^4\) as well as graphite and graphene\(^5-9\). Graphene offers a unique opportunity to extend such structural lubricity to the macroscale because it can be produced at television-screen dimensions\(^10\) and transferred onto arbitrary surfaces\(^11-13\) to reduce friction on a wide array of mechanical components. Indeed, recent experiments have already shown that graphene can be used to reduce friction of macroscopic steel-to-steel contacts\(^14-16\) as well as diamond-like carbon on SiO\(_2\)\(^17\).

Recent calculations have shown that gold nanocrystals on graphite possess unusually low friction\(^18,19\). Two friction regimes are predicted to exist at different speeds. At low speeds, nanocrystals on graphite are expected to possess higher friction, consistent with previous studies of thermal diffusion of gold on graphite\(^20\) and on graphene\(^21\). However, at high sliding speeds in the range of 100 m/sec, nanocrystals are expected to behave radically differently, with much smaller drag and, therefore, lower friction. Such high speeds are not easily accessible by atomic force microscopy (AFM)\(^22,23\), and the use of a quartz crystal microbalance (QCM) was proposed to confirm this enhanced lubricity predicted at high surface speeds\(^18,19\). QCMs oscillate in shear mode when driven at their resonant frequency. Their surface velocity is given by \( 2\pi f A_{\text{osc}}(2\pi ft) \), where \( A_{\text{osc}} \) is the amplitude, \( f \) is the resonant frequency and \( t \) is the elapsed time. The oscillation amplitude is given by \( A_{\text{osc}} = C \times Q \times V \), where \( C = 1.3 \, \text{pm/V} \), \( Q \) is the quality factor, and \( V \) is the driving oscillation voltage\(^24\). Peak velocities can reach m/sec with displacement amplitudes in the range of 1–10 nm. The high quality factors of QCMs make them extremely sensitive to mass adsorption and to changes in dissipation at their surfaces. In the formalism developed for analyzing viscous friction of adsorbates on QCMs\(^25,26\), the change in frequency and dissipation induced by adsorbates can be connected to the slip time, \( \tau_s \), which is the characteristic time required for sliding adsorbates to stop, by the formula

\[
\Delta \left( \frac{1}{Q} \right) = -4\pi\tau_s \Delta f.
\]
The slip time is related to the drag coefficient as $\tau_s = \rho / \xi$, where $\xi$ is the drag coefficient and $\rho$ is the mass per unit area of adsorbates. QCMs along with this formalism have been exploited to determine the frictional behavior of weakly adsorbed monatomic gases like Xe and Kr$^{25-27}$, as well as the friction and adhesion of micron-sized beads$^{28,29}$. The technique has also recently been used to measure friction of adsorbed gases on graphene$^{30-32}$ as well as on graphite$^{33}$. However, QCMs have not yet been used to measure the friction of nanometer-scale, crystalline adsorbates.

We observe that depositing gold nanocrystals on graphene-coated QCMs decreases the resonance frequency and increases the energy dissipation. The measured changes of frequency and dissipation induced by gold nanocrystals are used to determine the slip time of the nanocrystals on graphene using the framework previously developed for friction of adatoms$^{25,26}$. The determined slip time is found to be more than an order of magnitude higher than the value predicted for ballistic friction, confirming the enhanced lubricity predicted at high surface speeds. Our molecular dynamics calculations indicate that the observed lubricity exceeds the previous predictions because the interaction strength between gold nanocrystals and graphene is lower than the value used for those predictions.

**Results**

Gold is deposited using electron beam evaporation after stabilizing a QCM coated with graphene and a control QCM without graphene in an ultra-high vacuum (UHV) environment. The areal density of nanocrystals is determined using an AFM after QCM measurements to be $1.01 \pm 0.02 \times 10^{12}$ crystals/cm$^2$ as shown in Fig. 1a. This is nearly two orders of magnitude higher than the defect densities in graphene as determined from Raman spectroscopy, which was $1.9 \times 10^{10}$ defects/cm$^2$. As such, we expect the responses of the graphene QCM to be dominated by the interaction of nanocrystals with the graphene lattice. In AFM images, nanocrystals appear to be disk-shaped with large apparent lateral diameter and smaller height with the height ranging from 2.8 to 4.0 nm. The apparent shape is due to the convolution between the nanocrystals and the AFM tip shape. As shown in Fig. 1b, nanocrystals are found to be isotropic in shape from transmission electron microscopy (TEM).

Figure 2 shows the influence of electron beam evaporation on the resonance frequencies and energy dissipations of both graphene-coated QCM and the control QCM. The shutter for the evaporator is opened at $t \approx 5.2 \times 10^4$ sec and gold is deposited for 605 seconds at a rate of $1.6$ ng/(cm$^2$ sec), as determined by the frequency shift of the control QCM using the Sauerbrey equation$^{34}$. A striking difference can be observed in the energy dissipation at the graphene and control QCM. The dissipation in the graphene QCM is found to increase by $4.45 \times 10^{-6}$ upon gold deposition. On the other hand, the dissipation of the control QCM does not change as observed previously$^{26}$, consistent with inertial mass loading in which the adsorbed gold attaches rigidly. Precise knowledge of the change in frequency and dissipation enables us to determine the slip time of the gold nanocrystals using the formalism developed for viscous energy dissipation induced by adsorbates on QCMs$^{25,26}$.

The total frequency shift $\Delta f$ of the graphene QCM is given by the formula

$$\frac{\Delta f}{f} = - \frac{N \omega m_s}{A \pi Z_q} \left( \frac{1}{1 + \omega^2 \tau_s^2} \right),$$

where $f$ is the resonant frequency, $N$ is the total number of nanocrystals on graphene, $\omega$ is the angular resonant frequency of the crystal, $m_s$ is the average mass of an individual sliding nanocrystal, $A$ is the active area of the
crystal, $Z_q$ is the acoustic impedance of AT-cut quartz ($8.8 \times 10^6 \text{ kg m}^{-2} \text{s}^{-1}$), and $\tau_s = m/\xi$ is the slip time for sliding crystals, with $\xi$ being the drag coefficient. Similarly, the shift in the inverse quality factor of the QCM is

$$\Delta f = \frac{2N_0m_s}{fA\pi Z_q} \left[ \frac{\omega \tau_s}{1 + \omega^2 \tau_s^2} \right].$$

We assume all adsorbed nanocrystals participate in sliding, and, thus, contribute to the observed change in frequency and dissipation, justified by the low defect density of the graphene used for our study. The slip time $\tau_s$ can be calculated from the ratio of the shifts in frequency and dissipation for the graphene QCM:

$$\tau_s = \frac{1}{4\pi} \frac{\Delta (1/Q)}{\Delta f}. \quad (4)$$

We find the slip time to be 8.9 ns, with an oscillation amplitude of 11.4 nm and a peak surface speed of 35.6 cm/sec using our data. The measured slip time is over an order of magnitude higher than the slip time predicted for a smaller gold nanocrystal with a mass of $1.5 \times 10^{-22} \text{ kg}$ undergoing the ballistic friction behavior 18. Therefore, the measured value confirms the enhanced lubricity predicted for the nanocrystals at high speeds. The average mass of the nanocrystals can also be determined using the above formula to be $7.7 \times 10^{-22} \text{ kg}$. We find that this value is 17% smaller than the value calculated from the amount of gold deposited on the control QCM. Such discrepancy is not surprising since the sticking coefficient of gold on graphite has been determined to be less than 1 below monolayer coverage at room temperature 35. The average crystal diameter is determined to be 4.2 nm assuming each nanocrystal is spherical with a mass density of 19.3 g/cm$^3$, consistent with our AFM measurements.

Figure 3 shows the dependence of the response of the graphene QCM as a function of the oscillation amplitude, $A_{osc}$, in the range of 1.5 to 11.4 nm, which is accessible to our QCMs. The peak surface speeds vary from 4.7 to 35.6 cm/sec in this experimentally observable window. The slip time as a function of the oscillation amplitude can be determined again by using $\Delta f$ and $\Delta (1/Q)$ as discussed above. The slip time decreases at lower speeds but the predicted transition to a much lower slip time is not seen. This indicates that the predicted transition to high lubricity occurs below 4.7 cm/sec.

It is important to note that nanocrystals do not collide with each other during our measurements. The motion between gold nanocrystals and graphene QCM can be described by a differential equation 36:

$$m \frac{d^2 v_2}{dt^2} = -\xi [v_2 - v_1] + m\omega^2 (v_2 - v_1),$$

where $v_2$ is the velocity of nanocrystals and $v_1$ is the velocity of graphene QCM. As such, $v_1 = v_0 \cos(\omega t)$, where $v_0$ is the amplitude of the QCM surface velocity. The solution to this differential equation is given by:

$$v_2 = \frac{1}{m^2 + \omega^2} \left[ \xi v_0 \cos(\omega t) + \xi mv_0 \omega \sin(\omega t) \right].$$

\[ (6) \]
Relative velocity of gold nanocrystal on the graphene QCM is
\[ v_s - v_i = \frac{1}{\omega^2 \omega^2} \left( -\omega^2 \omega^2 v_0 \cos(\omega t) + \zeta m v_0 \omega \sin(\omega t) \right). \tag{7} \]

Relative displacement, \( d \), is
\[ d = \frac{1}{\omega^2 \omega^2 + \zeta^2} \left( -\omega^2 \omega^2 v_0 \cos(\omega t) + \zeta m v_0 \sin(\omega t) \right). \tag{8} \]

This can be written as
\[ d = \frac{m v_0}{\sqrt{\omega^2 \omega^2 + \zeta^2}} \sin(\omega t + \phi), \tag{9} \]
where the phase, \( \phi \), is given by
\[ \phi = \tan^{-1}\left( \frac{\zeta}{m \omega} \right). \tag{10} \]

Therefore, the amplitude of the motion of nanocrystals on the graphene QCM is proportional to the maximum amplitude of the surface velocity of the graphene QCM. The maximum sliding amplitude of nanocrystals with respect to graphene is 3.1 nm with the surface velocity amplitude of 35.6 cm/sec, the maximum used for our experiment. The range of diameters of nanocrystals determines the maximum phase angle range. We estimate the range of the phase to be 20 degrees using the diameter distribution of ±1 nm observed in previous measurements with similar deposition parameters\textsuperscript{21}. Since the mean distance between nanocrystals in our experiment is 10 nm, the oscillation amplitudes and phase differences between nanocrystals are insufficient to allow collisions.

The question remains on why we observe the enhanced lubricity that exceeds the previous prediction\textsuperscript{18,19}. We use molecular dynamics (MD) simulations to determine the answer. Our MD calculations output drag coefficients, which are inversely proportional to slip times. First, our calculations find that the drag coefficient to be independent of size for model nanocrystals ranging in size from 2 to 4.5 nm in diameter; results for two nanocrystals are shown in Fig. 4. Thus, the observed lubricity is not higher than expected because of the larger sizes of our nanocrystals. Instead, our theoretical simulations reveal that the observed lubricity exceeds the prediction due to the interaction strength between graphene and nanocrystals being lower than assumed in previous calculations\textsuperscript{18,19}. The interaction potential between these surfaces is typically described by the Lennard-Jones potential,
\[ \epsilon = \frac{\sigma}{4} \left( \frac{\sigma}{r} \right)^{12} - \left( \frac{\sigma}{r} \right)^6. \tag{11} \]

where \( \epsilon \) is the depth of the potential well or the interaction strength, \( \sigma \) is the distance at which the interatomic potential is zero, and \( r \) is the distance between atoms. The ballistic friction of gold nanocrystals on graphite was predicted using \( \sigma = 2.74 \text{ Å} \) and \( \epsilon = 22 \text{ meV} \textsuperscript{18,19} \). \( \sigma \) and \( \epsilon \) are expected to be dependent on materials and have not been determined experimentally for either the gold-graphene or gold-graphite interfaces. Previous theoretical calculations for the gold-graphite interface have used \( \epsilon \) ranging from 12.7 to 34.1 meV and \( \sigma \) ranging from 2.74 to 3.00 Å\textsuperscript{37–39}. We focus on \( \epsilon \) and how it affects the drag coefficient rather than on \( \sigma \) because a larger range of \( \epsilon \) is deemed reasonable for the gold-graphite system and \( \sigma \), with a narrower acceptable range, was found to have a much less significant effect in our preliminary MD simulations. As shown in Fig. 4, the drag coefficient \( \zeta \) increases with the interaction strength and \( \epsilon \) being lower than 22 meV can explain the observed lubricity that exceed the previous prediction. Since the measured quantities determine the slip time rather than the drag coefficient, we calculate the drag coefficient using the average mass and slip time as well as the expected variation.
in diameters. We find the drag coefficient to be $8.6 \pm 6.1 \times 10^{-14}$ kg/s at the peak surface speed of 35.6 cm/sec. Therefore, our simulation reproduces the experimentally-measured drag with $\varepsilon \approx 6 \sim 15$ meV as shown in Fig. 4.

We note that the interaction strengths are condition and material dependent and the values obtained here are not generally-applicable for graphene on arbitrary substrates. We conclude that the weaker interaction strength than previously anticipated in the prediction of the ballistic nanofriction is the cause for the observed high lubricity of nanocrystals.

In summary, we have measured the changes in frequency and dissipation induced by depositing gold nanocrystals on QCMs covered with graphene. Nanocrystals increase the dissipation of the QCM coated with graphene while leaving the dissipation of the control QCM without graphene unaffected. The measured change in dissipation and frequency induced by the gold nanocrystals can be understood in the framework developed for friction of adatoms on metal surfaces. The determined slip time of gold nanocrystals is found to be over an order of magnitude higher than the value predicted for the ballistic friction of gold nanocrystals on graphite, confirming the enhanced lubricity predicted at high surface speeds. We perform molecular dynamics calculations and show that the observed lubricity, which exceeds the previous prediction, is due to the interaction strength between gold nanocrystals and graphene being lower than estimated in the previous modeling studies. As discussed above, specific sliding distances can be inferred from our analysis of the experimental data. In-situ high-resolution microscopy should be able to directly confirm these distances and verify our analysis. Furthermore, the precision of our measurement of the drag coefficient is limited by the distribution in the size of nanocrystals. Future experiments with more control over nanocrystals will improve the capability to determine their drag coefficients using the QCM technique.

**Methods**

The control and graphene QCM are as 5 MHz AT-cut QCM blanks (ICM Mfg.). Electrodes are patterned on both sides using a 10 nm Cr adhesion layer followed by 100 nm of Cu, and then 80 nm of Au using thermal evaporation. The graphene-coated QCM is prepared by transferring graphene grown by low-pressure chemical vapor deposition on copper onto a metallized QCM using a conventional PMMA-assisted, wet transfer method. As such, graphene is on unreconstructed, polycrystalline gold surface. Both QCMs are then annealed in H$_2$/Ar at 350 °C for 3 hours at atmospheric pressure in order to clean the surfaces of the QCMs. Raman measurements produce an I$_D$/I$_G$ ratio of 0.074 and a graphene defect density of $1.9 \times 10^{10}$ defects/cm$^2$. The QCMs are finally placed into a UHV chamber with a base pressure of ~2 x $10^{-9}$ Torr. The crystals are vacuum annealed in situ at 180 °C for 8 hours prior to experiments.

QCM experiments are performed in UHV. Nanocrystals are formed by evaporating gold on graphene via e-beam evaporation. The control and graphene QCMs are placed next to each other and receive the same flux of gold. Both QCMs are then annealed in H$_2$/Ar at 350 °C for 3 hours at atmospheric pressure in order to clean the surfaces of the QCMs. Raman measurements produce an I$_D$/I$_G$ ratio of 0.074 and a graphene defect density of $1.9 \times 10^{10}$ defects/cm$^2$. The QCMs are finally placed into a UHV chamber with a base pressure of ~2 x $10^{-9}$ Torr. The crystals are vacuum annealed in situ at 180 °C for 8 hours prior to experiments.

QCM experiments are performed in UHV. Nanocrystals are formed by evaporating gold on graphene via e-beam evaporation. The control and graphene QCMs are placed next to each other and receive the same flux of gold. Both QCMs are then annealed in H$_2$/Ar at 350 °C for 3 hours at atmospheric pressure in order to clean the surfaces of the QCMs. Raman measurements produce an I$_D$/I$_G$ ratio of 0.074 and a graphene defect density of $1.9 \times 10^{10}$ defects/cm$^2$. The QCMs are finally placed into a UHV chamber with a base pressure of ~2 x $10^{-9}$ Torr. The crystals are vacuum annealed in situ at 180 °C for 8 hours prior to experiments.

Frequency and electronic amplitude are continuously monitored for both QCMs using an Agilent 53220A frequency counter. Quality factors of both the control and graphene QCM are determined by ring-down measurements using a Tektronix 2024B oscilloscope. The ring down time constant is extracted from the ring down curve and Q is determined via the relationship $Q = \pi f \tau$, where $f$ is the fundamental frequency of the QCM.

To image gold nanocrystals on graphene with TEM, gold is deposited onto CVD graphene on electron-transparent substrates in the same manner as described above for the QCM devices. The substrates consist of Si with thermally grown SiO$_2$ (800 nm) and Si$_3$N$_4$ (16 nm) in which thin (~1 um) windows are etched with KOH. After deposition of the graphene and gold, the bottom side of the windows is etched by placing the
chip over HF vapor to remove the oxide, leaving a thin nitride membrane. Samples are imaged in a Titan 80–300 FEG S/TEM at 300 kV at high spot size (low beam current) to minimize beam-induced damage on the sample.

AFM images are acquired in air at room temperature using a Bruker Dimension 5000 atomic force microscope operating in tapping mode in ambient conditions. We use the Supersharp silicon AFM tips fabricated by Mikromasch with tip radius of <1 nm for imaging (Mikromasch HR-Res/10-Cr-An).

The all atom simulations consist of a single gold nanocrystal on graphene. The nanocrystal is modeled as Au atoms in a truncated-octahedron geometry with approximate diameters between 2 and 4.5 nm. The nanocrystal is placed such that its (111) surface is in contact with graphene that has in-plane dimensions of 14.0 nm × 7.1 nm. The interatomic interactions within the gold are described by the Embedded Atom Model (EAM) and those within the graphene described by the Adaptive Intermolecular Reactive Empirical Bond Order (AIREBO) potential. The Lennard-Jones potential is used to model gold-graphene interactions and is given by Equation 11, \[ V_{\text{int}} = 4ε[(σ/\rho)^{12} − (σ/\rho)^{6}] \], where \( ε \) is the interaction strength, \( σ \) is the distance at which the interatomic potential is zero, and \( ρ \) is the distance between atoms. We ran simulations at a range of interaction strengths, \( ε \), to explore the effect of this parameter. The simulations are performed using LAMMPS simulation software with a time step of 1 fs, and the Nosé-Hoover thermostat is used to control the temperature at 300 K.

First, simulations are run with no externally applied force to characterize the diffusion behavior of the system. Diffusion speed for each nanoparticle diameter is calculated from the approximately linear slope of the increase in the center of mass displacement of the nanocrystal with time. During production simulations, the graphene is translated laterally at speeds between 10 and 500 m/s. The center of mass of the gold nanocrystal and force acting on it are recorded and then averaged over time intervals of 0.5 ns. The drag coefficient is then calculated from \( ζ = F/\Delta v \), where \( F \) is the average force on the gold nanocrystal in the direction that the graphene is translated and \( \Delta v \) is the difference between the sliding speed of the nanoparticle on the graphene in that same direction. The drag coefficient is calculated from the simulation only when the difference in the speed of the nanocrystal and graphene is greater than the diffusion speed for a given nanoparticle size, i.e. when the nanocrystal is sliding relative to the graphene.

References

1. Muser, M. H. Structural lubricity: Role of dimension and symmetry. Europhysics Letters, 66, 97–103 (2004).
2. Sacco, J. E. & Sokoloff, J. B. Free sliding in lattices with two incommensurate periodicities. Physical Review B, 18, 6549 (1978).
3. Sokoloff, J. B. Theory of energy dissipation in sliding crystal surfaces. Physical Review B, 42, 760 (1990).
4. Hirano, M., Shinjo, K., Kaneko, R. & Murata, Y. Anisotropy of frictional forces in muscovite mica. Physical Review Letters, 67, 2642 (1991).
5. Liu, Z. E. & et al. Observation of Microscale Superlubricity in Graphite. Physical Review Letters, 108, 205503 (2012).
6. Feng, X., Kwon, S., Park, J. Y. & Salmeron, M. Superlubric Sliding of Graphene Nanoflakes on Graphene. ACS Nano, 7, 1718 (2013).
7. Kawai, S. et al. Superlubricity of graphene nanoribbons on gold surfaces. Science, 351, 957 (2016).
8. Dinnwiedel, M. et al. Superlubricity of Graphite. Physical Review Letters, 92, 126101 (2004).
9. Koren, E., Lortscher, E., Rawlings, C., Knoll, A. W. & Duerig, U. Adhesion and friction in mesoscopic graphite contacts. Science, 348, 679 (2015).
10. Bae, S. et al. Roll-to-roll production of 30-inch graphene films for transparent electrodes. Nature Nanotechnology, 5, 574–578 (2010).
11. Li, X. S. et al. Large-Area Synthesis of High-Quality and Uniform Graphene Films on Copper Foils. Science, 324, 1312–1314 (2009).
12. Suk, J. W. & et al. Transfer of CVD-Grown Monolayer Graphene onto Arbitrary Substrates. ACS Nano, 5, 6916–6924 (2011).
13. Martins, L. G. et al. Direct transfer of graphene onto flexible substrates. PNAS, 110, 17762–7 (2013).
14. Berman, D., Erdemir, A. & Sumant, A. V. Few layer graphene to reduce wear and friction on sliding steel surfaces. Carbon, 54, 454–459 (2013).
15. Berman, D., Erdemir, A. & Sumant, A. V. Reduced wear and friction enabled by graphene layers on sliding steel surfaces in dry nitrogen. Carbon, 59, 167–175 (2015).
16. Berman, D., Erdemir, A. & Sumant, A. V. Graphene: a new emerging lubricant. Materials Today, 17, 31–42 (2014).
17. Berman, D., Deshmukh, S. A., Sankaranarayanan, S. K. R. S., Erdemir, A. & Sumant, A. V. Macroscale superlubricity enabled by graphene nanoscill formation. Science, 348, 1118 (2015).
18. Guerra, R., Tartaglino, U., Vanossi, A. & Tosatti, E. Ballistic nanofriction. Nat Mater, 9, 634–7 (2010).
19. Pisov, S., Tosatti, E., Tartaglino, U. & Vanossi, A. Gold clusters sliding on graphite: a possible quartz crystal microbalance experiment? Journal of Physics: Condensed Matter, 19, 305015 (2007).
20. Bardotti, L. et al. Diffusion and aggregation of large antimony and gold clusters deposited on graphite. Surface Science, 367, 276 (1996).
21. Liu, L. et al. Slow gold adatom diffusion on graphene: effect of silicon dioxide and hexagonal boron nitride substrates. Journal of Physical Chemistry B, 117, 4305 (2013).
22. Park, J. Y. & Salmeron, M. Fundamental Aspects of Energy Dissipation in Friction. Chemical Reviews, 114, 677–711 (2014).
23. Szulawska, I., Chandross, M. & Carpick, R. W. Recent advances in single-asperity nanotribology. Journal of Physics D: Applied Physics, 41, 123001 (2008).
24. Borovskiy, B., Mason, B. L. & Krim, J. Scanning tunneling microscope measurements of the amplitude of vibration of a quartz crystal oscillator. Journal of Applied Physics, 88, 4017–4021 (2000).
25. Krim, J., Solina, D. & Chiarello, R. Nanotribology of a Kr monolayer: A quartz-crystal microbalance study of atomic-scale friction. Physical Review Letters, 66, 181–184 (1991).
26. Watts, E., Krim, J. & Widom, A. Experimental observation of interfacial slippage at the boundary of molecularly thin films with gold substrates. Physical Review B, 41, 3466–3472 (1990).
27. Coffey, T. & Krim, J. Impact of Substrate Corrugation on the Sliding Friction Levels of Adsorbed Films. Physical Review Letters, 95, 076101 (2005).
28. Berg, S. & Johansmann, D. High Speed Microtribology with Quartz Crystal Resonators. Physical Review Letters, 91, 145505 (2003).
29. D’Amour, J. N. et al. Capillary Aging of the Contacts between Glass Spheres and a Quartz Resonator Surface. Physical Review Letters, 96 (2006).
30. Walker, M., Jaye, C., Krim, J. & Cole, M. W. Frictional temperature rise in a sliding physisorbed monolayer of Kr/graphene. Journal of Physics: Condensed Matter, 24, 424201 (2012).
31. Zhang, Y. N., Bortolani, V. & Mitsura, G. Influence of graphene coating on the adsorption and tribology of Xe on Au (111) substrate. Journal of Physics: Condensed Matter, 26, 445003 (2014).
32. Pierno, M. et al. Thermal lubricty of monolayer graphene on monolayer. Nanoscale, 6, 8062 (2014).
33. Kobayashi, H., Taniguchi, J., Suzuki, M., Miura, K. & Arakawa, I. Sliding Friction of Kr Films Adsorbed on Graphite. *Journal of the Physical Society of Japan*, **79**, 014602 (2010).
34. Sauerbrey, G. Verwendung von Schwingquarzen zur Wägung dünner Schichten und zur Mikrowägung. *Zeitschrift für Physik*, **155**, 206–222 (1959).
35. Arthur, J. R. & Cho, A. Y. Adsorption and desorption kinetics of Cu and Au on (0001) graphite. *Surface Science*, **36**, 641–660 (1973).
36. Sokoloff, J. B., Kriv, J. & Widom, A. Determination of an atomic-scale frictional force law through quartz-crystal microbalance measurements. *Physical Review B*, **48**, 9134 (1993).
37. Lewis, L., Jensen, P., Combe, N. & Barrat, J.-L. Diffusion of gold nanoclusters on graphite. *Physical Review B*, **61**, 16084 (2000).
38. Luedke, W. D. & Landman, U. Structure, Dynamics and Thermodynamics of Passivated Gold Nanocrystallites and Their Assemblies. *Journal of Physical Chemistry*, **100**, 13323–13329 (1996).
39. Neek-Amal, M., Asgari, R. & Rahimi Tabar, M. R. The formation of atomic nanoclusters on graphene sheets. *Nanotechnology*, **20**, 135602 (2009).
40. Silvestrelli, P. L. & Ambrosetti, A. van der Waals corrected DFT simulation of adsorption processes on transition-metal surfaces: Xe and graphene on Ni (111). *Physical Review B*, **91**, 195405 (2015).
41. Li, X. *et al.* Large-area synthesis of high-quality and uniform graphene films on copper foils. *Science*, **324**, 1312–4 (2009).
42. Ishigami, M., Chen, J. H., Cullen, W. G., Fuhrer, M. S. & Williams, E. D. Atomic structure of graphene on SiO2. *Nano Lett.*, **7**, 1643–1648 (2007).
43. Lucchese, M. M. *et al.* Quantifying ion-induced defects and Raman relaxation length in graphene. *Carbon*, **48**, 1592–1597 (2010).
44. Liu, L. *et al.* Slow gold adatom diffusion on graphene: effect of silicon dioxide and hexagonal boron nitride substrates. *J Phys Chem B*, **117**, 4305–12 (2013).
45. Foiles, S. M., Baskes, M. I. & Daw, M. S. Embedded-Atom-Method Functions for the Fcc Metals Cu, Ag, Au, Ni, Pd, Pt, and Their Alloys. *Phys. Rev. B*, **33**, 7983–7991 (1986).
46. Stuart, S. J., Tutein, A. B. & Harrison, J. A. A reactive potential for hydrocarbons with intermolecular interactions. *Journal of Chemical Physics*, **112**, 6472–6486 (2000).
47. Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular-Dynamics. *Journal of Computational Physics*, **117**, 1–19 (1995).

**Acknowledgements**

This work is based upon research supported by the National Science Foundation under Grant No. 0955625 (MLS, BTB, BDD and MI) and Grant No. CMMI-1265594 (CT and AM). BDD and MI were also supported by the Intelligence Community Postdoctoral Fellowship.

**Author Contributions**

M.S.L. performed the experiment, analyzed the data, and wrote the manuscript. C.T. and A.M. performed the theoretical simulations and wrote the theoretical portions of the manuscript. A.M. also helped to revise the manuscript. B.T.B. prepared graphene and QCMs necessary for the experiment. W.A.H. performed the TEM analysis. B.D.D. proposed the experiment and performed preliminary experiments to establish the feasibility. M.I. assisted in analyzing the data and helped to write the manuscript.

**Additional Information**

**Competing financial interests:** The authors declare no competing financial interests.

**How to cite this article:** Lodge, M. S. *et al.* Lubricity of gold nanocrystals on graphene measured using quartz crystal microbalance. *Sci. Rep.*, **6**, 31837; doi: 10.1038/srep31837 (2016).

This work is licensed under a Creative Commons Attribution 4.0 International License. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder to reproduce the material. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/

© The Author(s) 2016