Visualization of weak interactions between quantum dot and graphene in hybrid materials

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The mechanisms of the weak interactions within hybrid materials such as quantum dot (QD) and graphene (GR) have important implications for the design of related optoelectronic devices. We characterize the weak interactions in hybrid QD-GR systems using a non-covalent interactions approach. For a single Cd₃Se₃ QD with a core-cage structure, the intensity of the steric repulsive strain in every Cd-Se spatial four-atom ring of the cage surface is stronger than that of the inter-core-cage structure. Van der Waals (vdW) interactions occur within the cavity of the cage and within the six-atom rings of the cage surface. The spatial repulsion strain and attractive interactions play a key role in stabilizing the structure of the monolayer graphene. Interestingly, the spatial six-atom ring of the single QD change into spatial four-atom rings of the QD in the hybrid system, accompanied by the translation of vdW interactions into steric repulsive interactions. We conclude that the vdW interactions with π extensions and the weak attractive interactions within local areas between the QD and graphene together stabilize the integral structure of the hybrid QD-GR system. These results explain of the formation mechanism and the stabilization of the components in QD-GR hybrid materials.

Over the past several years, low-dimensional colloidal quantum dots (QDs) and graphene hybrid materials have aroused strong research interest because of their potential applications in novel optoelectronic devices; this potential arises from their unique optical and electronic properties. Colloidal QDs exhibit broad absorption spectra. Because they are zero-dimensional nanomaterials with obvious quantum confinement effect, their emission spectra can be easily tuned from the visible-light to the infrared-light region via the low-cost synthesis of QDs of different sizes. QD nanoclusters have been intensively investigated as promising materials for light-emitting diodes for full-colour displays and light-harvesting materials for solar cells and fluorescent sensors. By contrast, single-layer graphene, as a two-dimensional hexagonal honeycomb material, possesses high-speed charge carriers and exhibits low light absorption. Because of its extraordinary optical and electric properties, graphene is an excellent candidate for transparent electrodes. Therefore, graphene offers great prospects for complementing QDs in hybrid materials systems, and the mechanisms of energy and charge transfer from QDs to graphene in hybrid QD-GR structures have been intensively explored both experimentally and theoretically.

In hybrid QD-GR structures, graphene sheets are generally the substrate and QDs lie on them because of weak interactions with graphene. The weak interactions are necessary for forming stable structures including single QD, single-layer graphene and QD-GR hybrid materials; however, the characterization and correlation of low-dimension materials’ different weak interactions, which play a key role in stabilizing the structures, are not clear. In addition, understanding the compatible mechanisms of weak interactions within the hybrid QD-GR structures will be advantageous for designing and fabricating high-performance low-dimensional, integrated optoelectronic devices by combining QDs with graphene.

We can utilize a recently developed analysis method pertaining to non-covalent interaction (NCI) to observe and understand the different weak interactions within the hybrid QD-GR structures, including attractive interactions, vdW interactions and steric repulsive interactions. The NCI approach can be used to thoroughly analyse...
the peculiarity of different weak interactions of various inter- and intra-molecular and solid structures. The NCI theory is based on the dependence of the reduced density gradient $\text{RDG}(r)$ on the electron density $\rho(r)$:

$$\text{RDG}(r) = \frac{1}{2(3\pi^2)^{1/3}} \frac{|\nabla \rho(r)|}{\rho(r)^{4/3}}$$  \hspace{1cm} (1)$$

Furthermore, $\lambda_2$, which is the eigenvalue of the electron density Hessian matrix $\rho(r)$, is another important parameter in the NCI method. The NCI analysis method depends on the values of $\text{RDG}(r)$ and $\rho(r)$ from the regions of weak interactions in the 2D scatter graph, in which $\rho(r)$ is the horizontal ordinate and $\text{RDG}(r)$ is the vertical coordinate with relatively low numerical values, and the scatter distribution of $\text{RDG}(r)$ appears similar to tail feathers oriented towards the horizontal axis. Meanwhile, according to the function values of $\rho(r)$, the sign of $\lambda_2$ changes, so the quantity $\text{sign}(\lambda_2)\rho(r)$ serves as the new horizontal ordinate replacing $\rho(r)$. The attractive interactions are based on negative values of $\text{sign}(\lambda_2)\rho(r)$, and the repulsive interactions are based on positive values of $\text{sign}(\lambda_2)\rho(r)$, all with relatively large $\rho(r)$ values. The weak interactions actions occur as vdW interactions when the values of $\text{sign}(\lambda_2)\rho(r)$ approach zero, irrespective of the sign of $\lambda_2$. Under these circumstances, the 2D scatter graphs can be transformed into 3D colour graphs of RDG isosurfaces based on a colour scale representation of the numerical value range of the $\text{sign}(\lambda_2)\rho(r)$ values, enabling the weak interactions in the solid structure to be easily observed in 3D space. For the 3D colour graph of the RDG isosurfaces, the deeper blue colours indicate stronger attractive interactions, which correspond to the smaller negative numbers of the horizontal ordinate in the 2D scatter graph, and the deeper red colours indicate stronger repulsive interactions, which correspond to the larger positive numbers of the horizontal ordinate. The green colours indicate the vdW interactions, which correspond to numerical values close to zero regardless of the negative or positive horizontal axis direction. The colours between blue and green indicate gradually weaker attractive interactions, and the colours between green and red indicate gradually stronger repulsive interactions.

In this work, using the NCI approach, we systematically analysed the features of the weak interactions of single QD, single-layer graphene, and hybrid QD-GR structures on the basis of density functional theory (DFT) calculations. By visually observing various weak interactions, we elucidated their rule for maintaining stable structures of the single QD and single-layer graphene; we also observed a point where the characteristics of the weak interactions of the QD in the optimized hybrid QD-GR system differed from those of the single optimized QD. This difference was caused by the slight rearrangement in the structures of the QD with the fully relaxed geometric structures of the hybrid QD-GR system. However, a comparison of the single-layer graphene with the graphene of the hybrid QD-GR system revealed that the weak interactions were mainly the same. Furthermore, we obtained reliable conclusions about the $\pi$-extension vdW interactions and local-area weak attractive interactions that together contribute the key effects for stabilizing the integrated structures of the hybrid QD-GR materials.

Results

Structure model of the quantum dot, graphene and hybrid materials. In this work, the structure model of the optimized single QD as Cd$_{13}$Se$_{13}$ nanostructure is shown in Fig. 1(a); the QD is stable core-cage structure as confirmed proved by mass spectrometry. Notably, the bond lengths between the central Se atoms and the four nearby Cd atoms of the QD cage surface are 2.87 Å, 2.87 Å, 2.87 Å, and 2.89 Å, and the interval between the specified Cd and Se atoms is 4.13 Å, as marked on one of the Cd-Se spatial six-atom rings of the cage surface in Fig. 1(a). The electronic structure of Cd$_{13}$Se$_{13}$ QD has been extensively studied using first-principle methods; however, we seek to further elucidate the characterization of weak interactions in the core-cage structure of QD.

The structure model of the optimized single-layer graphene is quadrilateral, as shown in Fig. 1(b,c) with top and side views; this structure includes two armchair edges and two zigzag edges with H atoms linked to the edge C atoms. A similar hexagonal honeycomb structure for graphene was introduced in our previous work. The length and width of the quadrilateral graphene are 15.67 Å and 14.67 Å respectively, and the lattice constant is 1.42 Å, as shown in Fig. 1(b). Experiments and theoretical calculations have demonstrated the electronic structures of graphene with zigzag and armchair edges, and we have also further observed the features of the weak interactions within the graphene structure.

Utilizing the aforementioned structural model for the optimized QD and graphene, we combined QD with graphene to form a hybrid QD-GR structure by placing QD in the upper of quadrilateral graphene nanosheet using a DFT geometric relaxation computation, as shown in Fig. 1(d,e) with top and side views. By comparing the structure of the optimized single QD with the structure of the QD in the optimized hybrid QD-GR system, we observed a slight rearrangement of the QD structure in the hybrid system; we observed a similar result for graphene. The bond lengths between the central Se atoms of the QD core centre and four nearby Cd atoms of the QD cage surface of the hybrid QD-GR structure become 2.83 Å, 2.88 Å and 2.91 Å and 3.01 Å (cf. those of the single QDs). Notably, one of the Cd-Se spatial six-atom rings of cage surface in the single QD changes into a double Cd-Se spatial four-atom rings in the hybrid QD-GR structure; the length of the new bond between the specified Cd and Se atoms is 2.89 Å, which is marked among the double Cd-Se spatial four-atom rings of the cage surface in Fig. 1(e), in contrast to the single QD in Fig. 1(a). The geometric structure of graphene in the hybrid system appears to have a slightly bent and twisted surface as compared to the very flat structure of the single-layer graphene (Fig. 1(d) and (e)), similar to the phenomenon of a small ball placed on and bending a flat sponge. The distance between the bottom of the QD and the top of the graphene surface is approximately 2.5 Å.

Characterization of the weak interactions in single Cd$_{13}$Se$_{13}$ QD. The 2D scatter graph of single QD is illustrated in Fig. 2(a). To explore the weak interactions, we only focus on low numerical values of RDG, with a cutoff value of 0.3 a.u., and low values of the horizontal axis, $\text{sign}$$\lambda_2$$\rho(r)$, with an interval between $-0.01$ a.u. and
Figure 1. The optimized structure model. (a) Single Cd$_{13}$Se$_{13}$ QD with a core-cage structure. The bond lengths between the central Se atoms and four nearby Cd atoms of QD cage surface are 2.87 Å, 2.87 Å, 2.87 Å, and 2.89 Å, and the interval between the specified Cd and Se atoms is 4.13 Å. (b,c) Quadrilateral graphene with two armchair edges and two zigzag edges with top and side views, respectively. The length and width of the single-layer graphene are 15.67 Å and 14.67 Å, respectively, and the lattice constant is 1.42 Å. (d,e) Hybrid QD-GR structure with top and side views, respectively. The bond lengths between the Se atoms of the QD core centre and four nearby Cd atoms of the QD cage surface in the optimized hybrid QD-GR system become 2.83 Å, 2.88 Å and 2.91 Å and 3.01 Å. The length and width of the quadrilateral graphene with a slightly bent and twisted surface in the optimized hybrid QD-GR system are 15.66 Å and 14.64 Å, respectively.
Figure 2. The 2D scatter graphs of single QD and 3D colour graphs of RDG isosurfaces with a blue-green-red colour scale date range corresponding to the values of \( \text{sign}(\lambda_2)\rho(r) \) on the horizontal ordinate of the 2D scatter graph from \(-0.02\) a.u. to \(0.02\) a.u. (a) The 2D scatter graph corresponding to the values of \( \text{sign}(\lambda_2)\rho(r) \) on the horizontal ordinate for the weak interactions from \(-0.01\) a.u. to \(0.02\) a.u. (b) The 3D colour graph of the RDG isosurfaces with a numerical cutoff value of \(0.3\) a.u. (c,d) The 2D scatter graph corresponding to the values of \( \text{sign}(\lambda_2)\rho(r) \) for the weak interactions between \(0.013\) a.u. and \(0.02\) a.u. and the 3D colour graph of the RDG isosurfaces with a cutoff value of \(0.3\) a.u., respectively. (e,f) The 2D scatter graph corresponding to the values of \( \text{sign}(\lambda_2)\rho(r) \) for the weak interactions between \(-0.01\) a.u. and \(0.008\) a.u. and the 3D colour graph of the RDG isosurfaces with a cutoff value of \(0.36\) a.u., respectively.
0.02 a.u. in the 2D scatter graph, corresponding to the RDG distribution, which resembles a tail feather structure towards the horizontal axis within the black frame in Fig. 2(a). 3D colour graph of the RDG isosurfaces is shown in Fig. 2(b). Clear characterization of the weak interactions in different parts of the QD, requires analysis of the 2D scatter graphs in detail; we therefore decomposed the horizontal ordinate into three subsections in the 2D scatter graph, as follows:

First, we only kept the values of the RDG that correspond to the interval of numerical values of between 0.013 a.u. and 0.02 a.u. on horizontal ordinate, as shown in Fig. 2(c), and demonstrated the colour graph of the RDG in 3D space with a cutoff value of 0.3 a.u., respectively, (the inset shows the side view). (c) The 3D colour graph of the RDG isosurfaces with a cutoff value 0.6 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions of the 2D scatter graph between 0.014 a.u. and 0.024 a.u. (d) The 3D colour graph of the RDG isosurface with cutoff value of 0.5 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions of the 2D scatter graph between 0 a.u. and 0.013 a.u. (e) The 3D colour graph of the RDG isosurface with a cutoff value of 0.6 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions of the 2D scatter graph between −0.02 a.u. and 0 a.u.

Figure 3. The 2D scatter graphs of single-layer graphene and 3D colour graphs of RDG isosurfaces with blue-green-red colour scale data ranging from −0.02 a.u. to 0.02 a.u. (a,b) The 2D scatter graph corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions from −0.02 a.u. to 0.024 a.u. and the 3D colour graph of the RDG isosurfaces with cutoff value of 0.6 a.u., respectively, (the inset shows the side view). (c) The 3D colour graph of the RDG isosurfaces with a cutoff value 0.6 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) for the weak interactions in the 2D scatter graph between 0.014 a.u. and 0.024 a.u. (d) The 3D colour graph of the RDG isosurface with cutoff value of 0.5 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions of the 2D scatter graph between 0 a.u. and 0.013 a.u. (e) The 3D colour graph of the RDG isosurface with a cutoff value of 0.6 a.u. corresponding to the values of \( \text{sign}(\lambda_2) \rho(r) \) on the horizontal ordinate for the weak interactions of the 2D scatter graph between −0.02 a.u. and 0 a.u.

Peculiarity of the weak interactions in the single-layer graphene. We used the same method to demonstrate the 2D scatter graph of single-layer graphene in Fig. 3(a) and to show the visualization analysis of the 3D RDG isosurfaces in Fig. 3(b) with a cutoff value of 0.6 a.u., corresponding to the values on the horizontal ordinate between the interval from −0.02 a.u. to 0.024 a.u. in the 2D scatter graph. We analysed the peculiarity of the weak interactions in every section. The 3D colour graph of the RDG isosurfaces that correspond to interval
Features of the weak interactions in the hybrid QD-GR structure. The 2D scatter graph of the hybrid QD-GR structure is shown in Fig. 4(a), and the RDG distributions for the region of weak interactions are relatively complicated. To easily distinguish the roles of the weak interactions in the main region of the 2D scatter graph of the hybrid QD-GR structure, we unambiguously demonstrated the corresponding 3D colour graph of RDG isosurfaces. We translated the corresponding entire cube grid surrounding the whole QD-GR structure into two-part cube grid, and made the cube grid to surround the QD and graphene in the hybrid QD-GR system. We then plotted the 2D scatter graph of the QD in the hybrid QD-GR structure shown in Fig. 4(b). The corresponding 3D colour graph of the RDG isosurfaces with a cutoff value of 0.29 a.u. is shown in Fig. 4(c). This graph exhibits similar colours and shapes for isosurfaces compared to the graph of the single QD in Fig. 2(b), except for a few obvious differences. By comparing the geometric structure of the QD in the hybrid QD-GR system with single QD, we found that the geometric structure had slightly changed, but that the core-cage structures of the QDs were similar. One obvious difference was observed in that the new emerging double spatial four-atom rings of the QD in the hybrid system, shown in Fig. 1(e), replaced one of the spatial six-atom rings of the single QD, as shown in Fig. 1(a). On the basis of the NCI analysis, we found two red rice grain-shaped isosurfaces with steric repulsive interactions in the double spatial four-atom rings of the QD in the hybrid system, as shown in Fig. 4(c); these interactions are distinctly different from the vdW interactions of the spatial six-atom rings of the single QD, as shown in Fig. 2(h).

The 2D scatter graph of the graphene in the hybrid QD-GR system is shown in Fig. 4(d), and the 3D colour graph of the RDG isosurfaces with a cutoff value of 0.6 a.u. is presented in Fig. 4(e). By comparing Figs 3(a) and 4(d), we observed the phenomenon where the two 2D scatter graphs were approximately the same, and the 3D colour graphs were similar when comparing Figs 3(b) and 4(e), even if the spatial structure of the graphene in the hybrid QD-GR system was bent slightly more than the two-dimensional flat single-layer graphene.

To distinctly analyse the features of the 2D scatter graph of the hybrid QD-GR structure, we plotted the 2D scatter graph of the QD and graphene in the hybrid QD-GR system and that of the whole hybrid QD-GR structure in an overlap graph, as shown in Fig. 4(f). By excluding the contribution from the 2D scatter graph of the QD and graphene in the QD-GR system, we observe that the new weak interactions increased and that the new tail feathers distribution of the low numerical values of the RDG that point to the horizontal axis appear more prominently. On the basis of the aforementioned analysis of the 2D scatter graph and 3D colour graph of the RDG isosurfaces of the QD and graphene in the hybrid QD-GR system, we show exclusively in Fig. 4(g) the corresponding 3D colour graph of the RDG isosurfaces between the QD and graphene by shielding the 3D colour graph of the inter-QD and inter-graphene interactions in the hybrid QD-GR system. However, we clearly observe green large areas in the 3D colour graph of the RDG isosurfaces between the QD and graphene in the QD-GR hybrid structure in Fig. 4(g) with a cutoff value of 0.6 a.u., and elucidate that attractive interactions also appeared between the Se atoms of the lower part of the QD and the upper surface of the graphene, these interactions shown in light blue. Therefore, this figure visually exhibits the superposition effect of the weak vdW interactions with a π bond distribution and the localized attractive interactions.

Discussion
Because of the noticeable phenomena observation using the NCI analysis method, we can now discuss the character-ization of the weak interactions of the single QD, single-layer graphene, and the hybrid QD-GR structure.

In the case of single QD, by comparing the Cd-Se spatial-four atom rings to the spatial six-atom rings of the cage surface, we generalized that the strength of the weak interactions observably decreased, and that the strength of the weak interactions of the Se-Cd spatial four-atom rings within the cage of the QD was of medium intensity. In addition, the vdW interactions encircled the cavity inside the core-cage of the QD and provided a fundamental support frame for stabilizing the single QD structure. All of the aforementioned weak interactions together played an important role in stabilizing the single QD core-cage structure.

Regarding the single-layer graphene, we concluded that the strong steric stabilization due to repulsive strain in all six hexagonal rings of the C atoms stabilized the entire structural framework of the single-layer graphene. After observing the weak interactions of the armchair edges shown in Fig. 3(b), we observed two-coloured dark orange/blue isosurfaces, which revealed the fact that the weak repulsive and strong attractive interactions jointly functioned to stabilize the armchair edge structures of the single-layer graphene.

In the case of the hybrid QD-GR structure, the weak interactions of the QD in the hybrid system had slight difference and exhibited novel characteristics compared to the single QD. The QD in the hybrid system exhibited a slight structural rearrangement compared to the single QD, and observed an interesting phenomenon where altered weak interactions could verify the transformation of the structure. We observed that the spatial six-atom ring of the single QD shown Fig. 1(a), changed into double spatial four-atom rings for the QD in the hybrid system shown in Fig. 1(e); this change was accompanied by the vdW interactions becoming stericly repulsive interactions. Moreover, the intensity of the weak interactions of the QD in the hybrid structure, which is related to the colour and shape of the RDG isosurfaces in the 3D space, exhibited a slight difference in contrast compared...
Figure 4. The 2D scatter graphs of the hybrid QD-GR system and the 3D colour graphs of the RDG isosurfaces corresponding to a blue-green-red colour scale date range from $-0.02$ a.u. to $0.02$ a.u. (a) The 2D scatter graph of the hybrid QD-GR structure. (b,c) The 2D scatter graph of the QD in the hybrid QD-GR structure and the 3D colour graph of the RDG isosurface with a cutoff value of 0.29 a.u., respectively. (d,e) The 2D scatter graph of the graphene in the hybrid QD-GR structure and the 3D colour graph of the RDG isosurface with a cutoff value of 0.6 a.u., respectively, (the inset shows the side view). (f) The 2D overlap scatter graph of the QD, the graphene and hybrid structure in the hybrid QD-GR system. (g) The 3D colour graph of the RDG isosurface between the QD and graphene in hybrid QD-GR structure with a cutoff value of 0.6 a.u., (the inset shows the side view).
to that in the single QD, because the geometric structure partly rearranged after the hybrid QD-GR structure fully relaxed while maintaining the stabilization of the whole the core–cage structure. The weak interactions of the graphene in the hybrid system were similar to those of the single-layer flat graphene. Although slightly twisted graphene structure was observed in the hybrid system, the similar weak interactions could maintain the structural stabilization. However, the vdW interactions within the big π-extension areas and the weak attractive interactions within the local areas between the QD and graphene together played a key role in maintaining the stabilization of the integral structure of the hybrid QD-GR system.

In summary, we visually demonstrated the mechanisms of the weak interactions of single QD, single-layer graphene and hybrid QD-GR structure by utilizing the NCI approach and concluded that the attractive interactions, steric repulsive interactions, and vdW interactions cooperate in stabilizing the infrastructure of low-dimensional QD or graphene materials. Generally, in the case of single QD or QD in the hybrid system, similar weak interactions strongly affected the stability of the structure of the core–cage. Unexpectedly, we found that the weak interactions are advantageous for affirming the transformation of the QD structure in the hybrid system, in contrast to the single QD. By comparison with the single-layer graphene, we observed the phenomenon where a slight structural twist of the graphene in the hybrid system did not change the peculiarity of the weak interactions. In this work, we visually demonstrated the overlay effect of weak interactions due to the complex QD-GR structure, the superposition effect of π-extended vdW interactions and localized weak attractive interactions between the hybrid QD and the graphene system for stabilizing the integrated structure of the hybrid QD-GR system. This study improves existing knowledge of such complex materials at a fundamental level and promotes a deep understanding of the mechanisms of weak interactions for relevant integrated optoelectronic devices.

Methods

We optimized the geometric structure of low-dimensional QD and graphene materials via based DFT method by using the long-range hybrid functional B97X-D, which provides superior results with respect to non-bonding interactions. The basis set, LANL08, derived from the EMSL Quantum Chemistry Exchange Library was used for the C, O, and Se atoms, and the 6–31 g(d) basis set was applied for the C and H atoms. All of the calculations were conducted using the Gaussian 09 software package. The 2D scatter graph data and the cube grid data of the RDG surfaces of the different structures in all experiments with the same criteria, we used the VMD software to vary the colour scale date range corresponding to the horizontal ordinate in the 2D graphs from −0.02 a.u. to 0.02 a.u.

References

1. Chen, Z., Berclaud, S., Nuckolls, C., Heinz, T. F. & Brus, L. Energy Transfer from Individual Semiconductor Nanocrystals to Graphene. ACS Nano. 4, 2964–2968 (2010).
2. Konstantatos, G. et al. Hybrid graphene–quantum dot phototransistors with ultrahigh gain. Nat. Nano 7, 363–368 (2012).
3. Guo, X. F. et al. Fluorescence quenching of CdSe quantum dots on graphene. Appl. Phys. Lett. 103, 201909 (2013).
4. Ingrosso, C. et al. Photoactive Hybrid Material Based on Pyrene Functionalized PbS Nanocrystals Depositing CVD Monolayer Graphene. ACS Appl. Mater. Interfaces 7, 4151–4159 (2015).
5. Klimov, V. I. et al. Optical Gain and Stimulated Emission in Nanocrystal Quantum Dots. Science 290, 314–317 (2000).
6. Neeleshwar, S. et al. Size-dependent properties of CdSe quantum dots. Phys. Rev. B 71, 201307 (2005).
7. Kim, T.-H. et al. Full-colour quantum dot displays fabricated by transfer printing. Nat. Photonics. 5, 176–182 (2011).
8. Shirasaki, Y., Supran, G. J., Bawendi, M. G. & Bulovic, V. Emergence of colloidal quantum-dot light-emitting technologies. Nat. Photonics. 7, 13–23 (2013).
9. Seminon, O. E. et al. Peak External Photocurrent Quantum Efficiency Exceeding 100% via MEG in a Quantum Dot Solar Cell. Science 334, 1530 (2011).
10. Wang, R. et al. Colloidal quantum dot ligand engineering for high performance solar cells. Energy & Environmental Science 9, 1130–1143 (2016).
11. Freeman, R. & Willner, I. Optical molecular sensing with semiconductor quantum dots (QDs). Chem. Soc. Rev. 41, 4067–4085 (2012).
12. Geim, A. K. & Novoselov, K. S. The rise of graphene. Nat. Mater. 6, 183–191 (2007).
13. Mak, K. F. et al. Measurement of the Optical Conductivity of Graphene. Phys. Rev. Lett. 101, 196405 (2008).
14. Wang, X., Zhi, L. & Mullen, K. Transparent, Conductive Graphene Electrodes for Dye-Sensitized Solar Cells. Nano Lett. 8, 323–327 (2008).
15. Dong, C. et al. Intersubunit Electron Transfer (IET) in Quantum Dots/Graphene Complex: What Features Does IET Endow the Complex with? J. Phys. Chem. C 116, 15833–15838 (2012).
16. Zhang, D. et al. Understanding Charge Transfer at PbS-Decorated Graphene Surfaces toward a Tunable Photosensor. Adv. Mater. 24, 2715–2720 (2012).
17. Mengtao, S. & Peng Song, F. M. Photoinduced Electron Transfer in Organic Solar Cell: Principle and Applications (Science Press, 2017).
18. Chen, W. et al. Low temperature processed, high-performance and stable NiOx based inverted planar perovskite solar cells via a poly(2-ethylhexyl-2-oxazoline) nanodots cathode electron-extraction layer. Materials Today Energy 1–2, 1–10 (2016).
19. Sun, Z. et al. Infrared Photodetectors Based on CVD-Grown Graphene and PbS Quantum Dots with Ultrahigh Responsivity. Adv. Mater. 24, 5878–5882 (2012).
20. Lee, J. et al. Switching Individual Quantum Dot Emission through Electrically Controlling Resonant Energy Transfer to Graphene. Nano Lett. 14, 7115–7119 (2014).
21. Johnson, E. R. et al. Revealing Noncovalent Interactions. J. Am. Chem. Soc. 132, 6498–6506 (2010).
22. Contreras-García, J. et al. NCIPL0T: A Program for Plotting Noncovalent Interaction Regions. J. Chem. Theory Comput. 7, 625–632 (2011).
23. Lane, J. R., Contreras-Garcia, J., Piquemal, J.-P., Miller, B. J. & Kjaergaard, H. G. Are Bond Critical Points Really Critical for Hydrogen Bonding? J. Chem. Theory Comput. 9, 3263–3266 (2013).
24. Chaudret, R. et al. Unraveling non-covalent interactions within flexible biomolecules: from electron density topology to gas phase spectroscopy. Phys. Chem. Chem. Phys. 16, 9876–9891 (2014).
25. Miller, B. J., Lane, J. R. & Kjaergaard, H. G. Intramolecular OH···O interactions in alkenols and alkynols. Phys. Chem. Chem. Phys. 13, 14183–14193 (2011).
26. Kasuya, A. et al. Ultra-stable nanoparticles of CdSe revealed from mass spectrometry. Nat. Mater. 3, 99–102 (2004).
27. Del Ben, M., Haventh, R. W. A., Broer, R. & Stener, M. Density Functional Study on the Morphology and Photoabsorption of CdSe Nanoclusters. J. Phys. Chem. C 115, 16782–16796 (2011).
28. Azpiroz, J. M., Matxain, J. M., Infante, I., Lopez, X. & Ugalde, J. M. A DFT/TDDFT study on the optoelectronic properties of the amine-capped magic (CdSe)13 nanocluster. Phys. Chem. Chem. Phys. 15, 10996–11005 (2013).
29. Gao, Y. et al. Effect of ligands on the characteristics of (CdSe)13 quantum dots. RSC Adv 4, 27146–27151 (2014).
30. Wang, J. et al. Theoretical Investigations of Optical Origins of Fluorescent Graphene Quantum Dots. Sci. Rep 6, 24850 (2016).
31. Wang, J. et al. Optical advantages of graphene on the boron nitride in visible and SW-NIR regions. RSC Adv 6, 111345–111349 (2016).
32. Castro Neto, A. H., Guinea, F., Peres, N. M. R., Novoselov, K. S. & Geim, A. K. The electronic properties of graphene. Rev. Mod. Phys. 81, 109–162 (2009).
33. Fujii, S. et al. Role of edge geometry and chemistry in the electronic properties of graphene nanostructures. Faraday Discuss. 173, 173–199 (2014).
34. Zhang, X., Xin, J. & Ding, F. The edges of graphene. Nanoscale 5, 2556–2569 (2013).
35. Hohenberg, P. & Kohn, W. Inhomogeneous Electron Gas. Phys. Rev 136, B864–B871 (1964).
36. Chai, J.-D. & Head-Gordon, M. Long-range corrected hybrid density functionals with damped atom-atom dispersion corrections. Phys. Chem. Chem. Phys. 10, 6613–6620 (2008).
37. EMSL Basis Set Exchange Library. https://bse.pnl.gov/bse/portal.
38. M. Frisch Team (2009). R: A language and environment for quantum chemical computing. R Gaussian 09, Wallingford CT, USA. http://gaussian.com/.
39. Lu, T. & Chen, F. Multiwfns: A multifunctional wavefunction analyzer. J. Comput. Chem. 33, 580–592 (2012).
40. Humphrey, W., Dalke, A. & Schulten, K. VMD: Visual molecular dynamics. J. Mol. Graph. 14, 33–38 (1996).

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Author Contributions
F.M. and M.S. supervised the project, and S.C. and J.W. performed the calculations. M.S., S.C., J.W., Y.D., and F.M. analysed the data. S.C. and M.S. wrote the paper. All authors were involved in the discussions.

Additional Information
Competing Interests: The authors declare that they have no competing interests.

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