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Hexagonal High-entropy Alloys

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We report on the discovery of a high-entropy alloy (HEA) with a hexagonal crystal structure. Equiatomic samples in the alloy system Ho–Dy–Y–Gd–Tb were found to solidify as homogeneous single-phase HEAs. The results of our electron diffraction investigations and high-resolution scanning transmission electron microscopy are consistent with an Mg-type hexagonal structure. The possibility of hexagonal high-entropy alloys in other alloy systems is discussed.

Keywords: High-entropy Alloy, Structure, Transmission Electron Microscopy

High-entropy alloys (HEAs) constitute a novel field in materials science, currently attracting increasing research interest. The basic idea, pioneered by Yeh in 2004,[1] is to study alloys composed of multiple principal elements solidifying as metallic solid solutions on a simple crystal lattice. Usually, alloys with 4–9, occasionally up to 20 components [2] are considered.

In a multicomponent alloy, the total free energy is largely determined by the free energy of mixing, \( \Delta G_{\text{mix}} = \Delta H_{\text{mix}} - T \Delta S_{\text{mix}} \), where \( \Delta H_{\text{mix}} \) is the mixing enthalpy and \( \Delta S_{\text{mix}} \) the mixing entropy. In equimolar or near equimolar compositions, the mixing entropy can become dominant, stabilizing a random solid solution, if the elements are chosen such that the mixing enthalpy is neither too high positive (leading to segregation) nor too high negative (leading to the formation of ordered structures). In the ideal case, the resulting material is a perfectly disordered solid solution with a simple average crystal structure. HEAs are thus related to metallic glasses, but in contrast to the latter, they are thermodynamically stable, in particular at high temperatures.

Up to now numerous alloy systems have been reported in which HEAs exist. Without exception only HEAs with body-centered or face-centered cubic structures have been found. In this paper, we report on the observation of a HEA with a hexagonal crystal structure. We have prepared samples of equiatomic composition in the rare earth (RE)-system Ho–Dy–Y–Gd–Tb and characterized them by means of transmission electron microscopy (TEM), scanning electron microscopy (SEM), energy-dispersive x-ray diffraction (EDX) and scanning transmission electron microscopy (STEM).

We have prepared ingots of equiatomic Ho–Dy–Y–Gd–Tb in a high-frequency levitation furnace under 1 bar Ar atmosphere using 3N high-purity elements. Each ingot was remelted four times to ensure to achieve proper homogenization of the sample. Specimens for microstructural characterization were prepared by means of a dual-beam FEI Helios Nanolab 400S focused ion-beam (FIB) from the centers of the ingots. TEM was carried out using a Philips CM20 transmission electron microscope operated at 200 kV, SEM work using a JEOL 840 equipped with an EDAX energy-dispersive analytical system and STEM work using a probe-corrected FEI Titan 80–300 operated at 300 kV and equipped with a high-angle annular dark-field (HAADF) detector.

Figure 1(a) displays a scanning electron micrograph of the material using a composition-sensitive backscattered-electron detector. Figure 1(b) displays a STEM micrograph of the thin part of a typical FIB sample taken using a Z-contrast sensitive HAADF detector. Both images demonstrate that the sample is perfectly homogeneous, in particular there are no composition variations, no precipitates or secondary phases and no dendrites. We obtain these results consistently with FIB samples taken from various positions in the ingots. Note also that the cooling rate after levitation melting is sufficiently slow to allow for the formation of a homogeneous single phase. The average composition measured by EDX at eight different specimen positions

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is Ho 19.8 at%, Dy 20.0 at%, Y 20.4 at%, Gd 20.1 at%, Tb 19.7 at%. Within the experimental uncertainty this corresponds to the nominal equiatomic sample composition, and hence we conclude that the material solidifies congruently.

Figure 2(a) is an electron diffraction pattern taken at the [0 0 0 1] zone axis. The pattern displays perfect hexagonal symmetry, a number of reflections are indexed.

In order to determine the space group we follow a procedure described in [3]. Figure 2(b) is an overlay of two electron diffraction patterns at the [1 1 2 1] zone axis, a short-time exposure to display zero-order Laue zone reflections and a long-time exposure (inverted to enhance the weak spots) including first-order Laue zone reflections. The whole pattern has an m symmetry, which corresponds to the point group 6/mmm in a hexagonal system. Figure 2(c)–2(e) shows diffraction patterns at the [1 1 2 0], [4 1 5 0] and [1 0 1 0] zone axes, respectively, which are all perpendicular to [0 0 0 1].

The (0 0 0 1) reflection is visible at the [1 1 2 0] zone axis, but diminishes when tilting to [4 1 5 0] and essentially vanishes when tilting further to [1 0 1 0]. This indicates the presence of a 6_1 screw axis parallel to [0 0 0 1]. In the [1 1 2 0] pattern the (1 0 0 1) reflections are present, which rules out the P6_3/mcm case [4]. Consequently, the space group must be P6_3/mmc. Under stern scrutiny, an extremely weak residual intensity of the (0 0 0 1) reflection in the [1 0 1 0] zone can be seen. This may be due to a minor deviation from perfect disorder and is neglected in our analysis.

We have carried out tilting diffraction experiments on a single grain to determine the symmetry and angular distance of zone axes around [0 0 0 1]. The results are summarized in Figure 3, which displays the zone axes relevant for structure type determination within reach of the double-tilt goniometer stage. The [0 0 0 1] zone is surrounded by six (T 1 0 4) and six (T 2 T 6) zone axes (only half of which are shown).

The [T 1 0 4] zone is tilted by 15.24° with respect to [0 0 0 1] and shows a rectangular pattern that is repeated by five further zone axes rotated by 60° around [0 0 0 1]. The [T 2 T 6] zone is tilted by 17.60° with respect to [0 0 0 1] and shows a pattern with a different aspect ratio of the two reflections spanning the rectangular pattern. Five further equivalent zone axes are arranged around [0 0 0 1] rotated by angles of 60°. The dark lines represent the Kikuchi lines as seen in the TEM. The arrangement of the zone axes, as well as the Kikuchi lines, perfectly reproduces the hexagonal structure. A further zone axis displaying an almost hexagonal pattern, [T 2 T 3], which is tilted by 32° with respect to [0 0 0 1] was recorded. Note that some of the diffraction patterns contain very weak additional reflections, the origin of which is not clear. They may be due to double diffraction, minor deviations from perfect disorder or electron diffraction taking place in neighbored grains. These reflections were not taken into account in our analyses.

All zone axes, Kikuchi lines and reflections can consistently be indexed on the basis of a hexagonal structure. We compared calculated and experimental tilting angles of different zone axes as well as distances of reflections from the direct beam R_{hkil}. For the latter, we compared the ratio of R_{hkil} values of reflections spanning a diffraction pattern to the corresponding calculated d_{hkil} ratio. Due to the relationship R_{hkil}d_{hkil} = const, where the imprecisely known constant is given by the electron wavelength and the camera length of the microscope, these ratios should inversely correspond. Good agreement could be achieved using the lattice parameters \(a = 361\) pm and \(c = 569\) pm. These lattice
parameters correspond to the weighted average of the parameters of the constituting elements. A comparison of the experimental and calculated quantities using these parameters is presented in Table 1.

Figure 4 shows STEM micrographs, which were slightly FFT-filtered for high-frequency noise reduction. Figure 4(a) was taken along the [0 0 0 1] direction and in consistency with an Mg-type structure displays a pattern of interconnected hollow hexagons. The inset is an FFT of the image also reflecting the hexagonal structure. Figure 4(b) was taken along [1 1 2 0] and the FFT in the inset corresponds to the diffraction pattern in Figure 2(c). The image is also consistent with an Mg-type structure. In particular, the atomic arrangement along this direction excludes a $P6_3/mcm$ space group, which would lead to a pattern of paired atomic rows parallel to the [0 0 0 1] direction. This significantly differs from the almost hexagonal pattern expected for the $P6_3/mmc$ space group, which directly corresponds to the experimentally observed HAADF-STEM image.

This observation is consistent with our electron diffraction results. Both images, which were taken with a Z-contrast-sensitive HAADF detector, show that also on this small scale the material is perfectly homogeneous. There is no indication of precipitation or ordering.

The lattice parameters directly measured from the image amount to $a = (363 \pm 30)$ pm and $c = (566 \pm 20)$ pm, which is in agreement with the weighted average of the parameters of the constituting elements. It was observed earlier that the $a$-lattice constant in cubic HEAs follows a rule of mixtures.\cite{5} Our results indicate that a rule of mixtures also applies to the $c$-lattice parameter and the $c/a$ ratio.

Our electron diffraction and STEM results are consistent with an Mg-type hexagonal structure. That is, the unit cell has the space group $P6_3/mmc$ (No. 194) and two atoms per unit cell, on the $(1/3, 2/3, 1/4)$ position and its symmetric equivalent. The structure of the HEA is identical to the structures of the constituting elements, which are also of Mg-type.
Figure 3. Arrangement of zone axes and corresponding electron diffraction patterns, indexed according to a hexagonal Mg-type structure. The lines correspond to Kikuchi lines as seen in the TEM. Only half of the patterns surrounding [0 0 0 1] are shown. The indicated angle between [12 13] and [12 16] is not to scale as indicated by the broken lines.

Criteria for the formation of HEAs are commonly discussed in terms of radius differences and a parameter $\Omega$ referring to the thermodynamic properties of the alloy.\[6\] The radius difference $\delta r = \sqrt{\sum_i c_i (1 - r_i / r)^2}$, where $r_i$ are the element radii, $c_i$ the mole percentages and $r$ the weighted average radius, should be as small as possible. A value below about 6.5% for HEAs in general and below 3.8% for single-phase HEAs \[7\] is required. In our case $\delta r = 0.77\%$. The thermodynamic parameter $\Omega = T_m \Delta S_{mix} / |\Delta H_{mix}|$, where $T_m$ is the weighted average melting temperature, $\Delta S_{mix}$ the mixing entropy and $\Delta H_{mix} = \sum_{i,j} c_i c_j H_{ij}$,\[6\] should exceed 1.1 (which means that the entropy contribution to the free energy should dominate the enthalpy).

Since the alloy investigated is equiatomic, $\Delta S_{mix}$ reaches the maximum value $1.61 R$,\[1\] where $R = 8.314$ J K$^{-1}$ mol$^{-1}$ is the gas constant. $\Delta H_{mix}$ calculated using values from the tables provided by Takeuchi and Inoue \[8\] amounts to 0 kJ mol$^{-1}$. For Ho–Dy–Y–Gd–Tb not only the sum of the mutual mixing enthalpies is zero,
but each individual component $H_{ij} = 0 \text{kJ mol}^{-1}$ for all $i$ and $j$. The alloy thus fulfills an even stronger formation criterion. Formally, taking the calculated values for $\Delta H_{\text{mix}}$ [8] into account, the parameter $\Omega$ in our case diverges.

Further criteria supporting HEA formation are equal crystal structures, a high mutual solubility in the binary phase diagrams of all constituting elements and, from a practical point of view, close melting points. All formation criteria are ideally fulfilled for the system investigated.

Note that the same is true for numerous further RE-elements. Similarly positive conditions are present for La, Er, Tm, Lu, Pr, Pm and Nd. If we exclude Pm due to its radioactivity, in total we are left with 11 practically usable elements for which we expect the formation of hexagonal HEAs. Hence, HEAs with higher numbers of components up to 11 and numerous combinations should be possible. The number of possible equiatomic five-element HEAs is 462, and altogether 1486 different HEAs with 5–11 different elements can be combined. The elements Ho, Dy, Y, Gd and Tb used for the alloy investigated in this work, which can be considered a feasibility study, were chosen more or less arbitrarily from the potential candidates due to their immediate availability in our stock. We should point out that some of the elements used undergo a high-temperature transition from hexagonal to cubic structure at 95% (Gd and Tb) and 98% (Dy and Y) of their melting point. The exclusive use of elements that have a hexagonal structure up to their melting point may lead to a larger grained structure. This, however, would limit the system to the four elements Er–Tm–Lu–Ho.

The list can probably be further extended by taking into account elements that have a different crystal structure but also similar radii and low mixing enthalpies with the elements mentioned above. Ce, for example, shows high solubility with all RE-elements (with the presence of a miscibility gap, however) and mixing enthalpies between 0 and 1 kJ mol$^{-1}$. The same seems to hold for Sm, as far as phase diagrams are available.

We have chosen an equiatomic alloy composition for the present work, but we expect that due to the similarity of the constituting elements and hence generous compliance of the formation criteria, the existence ranges of the HEAs are very wide. The production of single-phase ingots with different compositions should therefore also be possible. This expected tolerance to composition variation may open up the possibility to form single-phase HEAs using Mischmetall, which is a more or less undefined alloy of RE-elements in various naturally occurring proportions. Since Mischmetall is considerably cheaper than high-purity single RE-elements, this would eliminate the economical disadvantage of the RE-systems under consideration.

The hexagonal HEAs presented may offer a unique chance to study the magnetism of RE-systems. Mainly related to their 4f electron configurations, RE-elements possess highly complex magnetic behavior displaying a wide variety of properties.[9] The systems presented are unique in the sense that they are topologically ordered but possess random bonds. In the present HEA systems, the included elements and the composition can most freely be varied at constant structure, which may allow for insightful comparative measurements. Furthermore, hexagonal HEAs, including Tm, Yb and Ce, may provide a way to study heavy-fermion behavior in a disordered system.

The hexagonal high-entropy systems also include the possibility to incorporate intentional second phases, that is, for the increase in strength, high-temperature applicability, etc. Potential candidates are Yb, Eu, Zr and Hf, which have a high melting temperature and a high positive mixing enthalpy with the RE-elements considered. The mixing enthalpies with these elements are between 6 and 18 kJ mol$^{-1}$, which will lead to segregation.

We should also point out that recently Gao and Alman [10] predicted the existence of a hexagonal HEA in the system Co–Os–Re–Ru. In this system, the formation criteria are indeed well fulfilled and all constituting elements are mutually soluble. The drawback of this system is that Os reacts with oxygen at room temperature forming the highly toxic osmium tetroxide. Furthermore for the elements proposed, the melting points are strongly different (1768 K (Co) vs. 3459 K (Re)) making the growth procedure practically difficult. Further candidates along these lines are Co–Re–Ru–Tc or the five-element system Co–Re–Ru–Tc–Os, both of which involve the radioactive element Tc.

In conclusion, in this paper we report on the observation of a HEA in the Ho–Dy–Y–Gd–Tb alloy system. Our samples are homogeneous and single-phased, and of hexagonal Mg-type structure.

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