Tethered multifluorophore motion reveals equilibrium transition kinetics of single DNA double helices

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We describe a tethered multifluorophore motion assay based on DNA origami for revealing biomolecular reaction kinetics on the single-molecule level. Molecular binding partners may be placed at user-defined positions and in user-defined stoichiometry; and binding states are read out by tracking the motion of quickly diffusing fluorescent reporter units. Multiple dyes per reporter unit enable single-particle observation for more than 1 hour. We applied the system to study in equilibrium reversible hybridization and dissociation of complementary DNA single strands as a function of tether length, cation concentration, and sequence. We observed up to hundreds of hybridization and dissociation events per single reactant pair and could produce cumulative statistics with tens of thousands of binding and unbinding events. Because the binding partners per particle do not exchange, we could also detect subtle heterogeneity from molecule to molecule, which enabled separating data reflecting the actual target strand pair binding kinetics from falsifying influences stemming from chemically truncated oligonucleotides. Our data reflected that mainly DNA strand hybridization, but not strand dissociation, is affected by cation concentration, in agreement with previous results from different assays. We studied 8-bp-long DNA duplexes with virtually identical thermodynamic stability, but different sequences, and observed strongly differing hybridization kinetics. Complementary full-atom molecular-dynamics simulations indicated two opposing sequence-dependent phenomena: helical templating in purine-rich single strands and secondary structures. These two effects can increase or decrease, respectively, the fraction of strand collisions leading to successful nucleation events for duplex formation.

Significance

Understanding cellular functions and dysfunctions often begins with quantifying the interactions between the binding partners involved in the processes. Learning about the kinetics of the interactions is of particular importance to understanding the dynamics of cellular processes. We created a tethered multifluorophore motion assay using DNA origami that enables over 1-hour-long recordings of the statistical binding and unbinding of single pairs of biomolecules directly in equilibrium. The experimental concept is simple and the data interpretation is very direct, which makes the system easy to use for a wide variety of researchers. Due to the modularity and addressability of the DNA origami-based assay, our system may be readily adapted to study various other molecular interactions.

Author contributions: H.D. designed research; M.S. performed research; M.Z. designed and performed MD simulations; M.S. analyzed experimental data; and M.S., M.Z., and H.D. wrote the paper.

The authors declare no conflict of interest.

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nanotechnology (37–39) and established a tethered particle assay for revealing bimolecular reaction kinetics that addresses successfully all of the above-mentioned issues.

Our current understanding of the kinetics of DNA hybridization mainly stems from studies of ensemble relaxation dynamics upon temperature changes, shock waves, or concentration jumps (40–49). Previous single-molecule fluorescence measurements have enabled directly observing hybridization and dissociation reactions in equilibrium (50–53) and have yielded more direct insight into how external conditions influence the underlying processes. Experimental data shedding light on how sequence controls the elementary reaction directions of double-helical DNA domain formation and dissociation are still scarce (49, 54), but such data may help making more informed decisions in the design of DNA-based biosensors, dynamic DNA nanodevices, and DNA computing circuits. It may also contribute to understanding the dynamics of DNA double helices in cellular contexts. We thus applied our assay to acquire quantitative data for DNA hybridization and dissociation reaction kinetics. We obtained these data through direct single-molecule observations of repeated binding and unbinding transitions of DNA single-strand pairs in unperturbed, true equilibrium.

To obtain qualitative insights into the molecular origins of our experimental results, we complemented them with all-atom molecular-dynamics (MD) simulations. A variety of simulation models with varying resolutions and parameters has been previously developed that allow studying reversible DNA hybridization and dissociation (55–57). Except for atomistic MD simulation studies of base pair opening and closing (fraying) at double-strand termini (58), the process of DNA hybridization has so far been studied by simulations employing a coarse-grained (CG) representation of the DNA partner molecules (54–57, 59, 60). CG models have been used to study the thermodynamics of different DNA sequences (59) and the kinetics of hybridization for long uniform sequences (55). However, CG models are parameterized to form dsDNA as a global optimum on a very smooth energy landscape and reproducing experimental stability. During the process of double-strand formation, DNA partners may form numerous non-Watson–Crick type hydrogen-bonding contacts and noncanonical intermediate motifs, which may not be well represented in a CG model without detailed atomistic interactions such as hydrogen bonds. We thus present here all-atom MD simulations in implicit solvent of reversible hybridization and dissociation of DNA duplexes.

Results

Establishing a Tethered Multifluorophore Motion Assay. We used standard multilayer DNA origami design methods (38, 61–63) and constructed two fluorescently labeled reporter units with radius of gyration on the scale of 15 nm to construct our upgraded TPM assay (Fig. 1A). To ensure high brightness and to prolong the observation time in single-particle fluorescence microscopy, we attached 20 copies of the organic dyes cyanine-3 and cyanine-5 onto each reporter unit, respectively (Fig. 1B and C). The reporter units serve the purpose of anchoring the fluorescent dyes onto a structurally well-defined particle while maintaining a minimum interdy distance to suppress quenching. Furthermore, one of the two reporter units was functionalized

![Diagram](image-url)
for stable immobilization of this unit on microscope glass slides with up to six biotin–NeutrAvidin connections (see SI Appendix, Figs. S1–S4 for details of the reporter unit design). We connected the two reporter units using a double-stranded DNA tether having single-strand nicks every 42 bp. This design allows attaching molecules at specific sites within the tether by exchanging particular oligonucleotides with their appropriately modified counterparts (Fig. 1D).

In the work presented here, two DNA single strands branch off from the tether at distances of L1 and L3 bp, respectively, counting from each reporter unit, which leaves a tether segment of length L2 base pairs between the two single strands. In addition to polythymine stretches that promote accessibility and orientation randomization, the two DNA single strands contained the complementary sequence motifs A and A'. The two single strands may thus form a double-helical DNA domain whose hybridization and dissociation is coupled to looping and unlooping, respectively, of the segment L2. In the bound state, the two fluorescent reporter units are separated with a short tether L1 + L3 base pairs long, while in the dissociated state of the bimolecular reaction under study the tether lengthens to L1 + L2 + L3, thereby extending the range of diffusive motion of the mobile reporter unit. We tested two geometries for anchoring the DNA single-strand targets within the tether system: proximal attachment, where both targets are anchored in close vicinity of the reporter units (L1 = 0 bp; L3 = 60 bp), and distal attachment of the target strands away from the reporter units, with L1 and L3 having ~300 bp length.

Similar as in previously described tethered (single) fluorophore motion assays (6, 25), for adequately chosen L2, it is possible to detect the bound and unbound states of the molecular system under study by tracking the motion of individual mobile reporter units using a fluorescence microscope (Fig. 1E and Movie S1) and discriminating intervals of lower and higher mobility, respectively. Because of the tethering, reversible hybridization and dissociation of the same pair of DNA single strands may be observed (Fig. 1 F and G). We acquired data using stroboscopic illumination (6) with alternating laser excitation (64) in a total internal reflection fluorescence microscope (TIRFM). The data allowed determining with subdiffraction precision the position of the mobile reporter unit relative to the immobilized unit using centroid tracking (65, 66), independent of the binding state. The spot tracking leads to trajectories of XY displacement over time of the mobile reporter unit relative to its mean position (Fig. 1G and SI Appendix, Fig. S5). The up to 75-min-long time traces reveal the relevant conformational states per single particle. These states include the designed hybridized conformation with looped tethers, leading to periods with small position fluctuations, and the dissociated conformations that are characterized by larger displacements.

For the analysis, we classified the single-particle displacement–time traces using maximum-likelihood hidden-Markov modeling (HMM) (67–69), and then determined the dwell times of the individual particles in the hybridized and dissociated states. Photobleaching of the fluorophores leads to decreasing signal-to-noise ratio (SNR) over time, which affects the particle tracking accuracy. The effect was included in our hidden-Markov treatment. For details, see SI Appendix, Materials and Methods and Figs. S6–S8. The prolonged illumination could potentially also damage the reporter units, the tether, or the reactant pair. However, the distributions of lifetimes that we obtained from consecutive intervals of 15-min length match closely (SI Appendix, Fig. S9). The lack of a time-dependent effect on the lifetimes indicates the absence of photoinduced alteration of sample behavior. Occasionally, we observed off-target binding to sticky patches on the microscope slides (SI Appendix, Fig. S10), which we also accounted for.

Tethered Multifluorophore Motion Resolves Molecular Heterogeneity.

In our assay, molecular heterogeneity in a sample may be discovered by acquiring many single-particle recordings, extracting particle displacement–time traces, and determining the average dwell times in unbound and bound states for each particle. For DNA oligonucleotides prepared by chemical synthesis as we studied them in this work, we may expect molecular heterogeneity stemming for example from chemical truncations. Preparing a scatter plot of the determined mean bound vs. mean unbound dwell times reveals multiple data point clusters, as exemplified with data that we acquired with a sample featuring two strands A and A' that can form an 8-bp-long double-helical DNA domain with sequence CCTCCTCC-GGAGGAGG (Fig. 2A). There is a main population of single-particle recordings that exhibited similar kinetic properties, but there were also particles that had substantially shorter bound-state lifetimes. Also, some particles took much longer on average to rebind but had similar bound-state lifetimes as the main population. Last, there were also a few particles that had both longer rebinding and shorter bound-state lifetime. Exemplary single-particle recordings from each of the scatter plot clusters clearly show that the respective particles exhibit quite distinct behavior, which must originate from molecular differences (Fig. 2B).

We attribute the population of particles with substantially shorter mean bound dwell times compared with the main population to particles having defective interaction sequences A and A' stemming from truncated synthesis products. This interpretation is supported by data obtained from experiments with a 9-bp motif CAGAGAGGCGTCTCTGG and an 8-bp motif CAGGAACCGTGTCTCTGG in the proximal attachment geometry. Short bound-state dwell time outliers of the 9-bp variant behave similarly to the main population of the 8-bp variant (Fig. 2C and SI Appendix, Fig. S11). We attribute long unbound-state dwell time outliers to particles with defects in our reporter units that lead to reduced accessibility of the molecular binding partners, which is particularly relevant for the proximal attachment geometry.

To provide an objective criterion for classifying the individual particles into main population and outliers, we use a probability-thresholding approach. Each single-particle recording is characterized by N dwells in each of the two states (bound and unbound) with stochastically distributed durations. For the purpose of sorting particles, we assume that the individual dwells follow single-exponential probability density distribution with global rate parameters. The probability for observing a particular sum of N dwell times in each state based is then given by an Erlang distribution. A particle was declared an outlier if, in either of the two states, its sum of dwell times was within the far tails of the distribution (<2/1,000,000 probability; Materials and Methods). The fraction of particles that were discarded as outliers by this approach varied between a few percent and up to 30%, depending on the sample.

Analysis of histograms derived by pooling all recorded individual single-particle dwell times in bound and unbound states from particles sorted into the main population (Fig. 2D) reveals that the data from the main population obey nearly ideally single-exponential decays, which strongly argues for homogeneity. The shape of the histogram for particles declared as outliers cannot be explained by a single-exponential decay. Instead, it reflects a mixture of processes having different stochastic behavior. Simply pooling all data into one class, as it would be unavoidable in ensemble measurements (49) and difficult to avoid in single-molecule assays with binding-partner exchange (51–53, 70), can lead to substantial errors in the determination of the kinetic rates of the target process under study (Fig. 2D). For instance, in the case of the 9-bp double-helical DNA domain, including outliers into the statistics would result in underestimating the hybridization rate by about 30%, and overestimating the off-rate by about 45%.
Tether Length and Anchor Sites of Reactants Influence On-Rate, but Not Off-Rate. The length of the looping tether will directly affect the rate of duplex formation by influencing how frequently the two molecular targets will diffusively hit each other, similar to how the concentrations of reactants influence the rate at which molecules randomly collide. Regarding the bound states, it is conceivable that the forces that counteract looping could also cause accelerated unbinding of the duplex, similar to the way pulling on DNA duplexes in atomic force microscopy or optical tweezers can induce helix melting and strand dissociation (71). To quantify the effect of tether length on the binding kinetics, we studied exemplarily the reversible hybridization and dissociation of an 8-bp-long DNA duplex with sequence CAGGAACG:CGTTCCTG using three different tether lengths in the distal attachment geometry (Fig. 3) and using five tether lengths in the proximal attachment geometry (SI Appendix, Fig. S12). On the level of single-particle position time traces, it is readily apparent that increasing the tether length leads to an increased duration of the heavily fluctuating, unbound state (Fig. 3A–C). We collected many single-particle displacement–time traces from fluorescence movies, separated outliers from the main species as described above, and computed the average time each analyzed particle spent in bound vs. unbound states. The scatter plots shown in Fig. 3D show these data pooled from hundreds of particles and reflect slower rebinding kinetics for longer tether length. By contrast, the unbinding kinetics has negligible dependence on tether length.

We pooled the dwell times each single particle spent in unbound and bound states and computed lifetime histograms. The resulting distributions containing thousands of single-duplex hybridization and dissociation events from several hundred independent single-particle recordings are virtually indistinguishable from single-exponential decays (Fig. 3E). Therefore, our tethered particle system realizes a two-state system that is described by two characteristic transition rate constants. Possible intermediates such as partially hybridized states either do not occur or have lifetimes below our detection limit. The observed behavior is consistent with the nucleation-zippering model of DNA hybridization (72). The dependence of the on-rate (inverse of the mean dwell time particles spent in the unbound states) on tether length (Fig. 3F, Left) may be explained with a simplified model of the entropic and enthalpic looping penalties according to $k_{\text{on}} \sim N^{-3/2}e^{-\Delta A}$, where $N$ is tether length in base pairs and $A$ is a constant (see Materials and Methods for details). The model resembles the previously reported $j$-factor dependence of DNA duplex length (73). The average off-rate was of the mean dwell time particles spent in the unbound states) on tether length (Fig. 3F, Right) is a constant (see Materials and Methods for details). The model resembles the previously reported $j$-factor dependence of DNA duplex length (73). The average off-rate was $\sim 0.05 \text{ s}^{-1}$ independent of tether length (Fig. 3F, Right).

We found that the distal attachment geometry yielded faster rebinding kinetics compared with proximal attachment of the two target strands (SI Appendix, Fig. S12). Presumably, placing the two targets at some distance from the reporter units alleviates steric exclusion effects and reduces constraints regarding the relative orientation for productive binding events. The distal geometry is then more similar to unrestricted binding events in solution. SI Appendix, Table S1 provides a summary of all experimentally determined rates, as well as the sizes of the corresponding datasets.

Concentration of Monovalent Salt Affects On-Rate, but Not Off-Rate. We carried out measurements on equilibrium duplex hybridization and dissociation as a function of salt concentration from physiological 0.15 mol/L up to 1 mol/L sodium chloride. We performed three sets of experiments with three different tether lengths.
Fig. 3. Kinetics of duplex formation and dissociation for three different tether lengths. (A) Typical particle trajectory of $r = \sqrt{\Delta x^2 + \Delta y^2}$ over time. Duplex CAGGAACG:CGTTCCTG, 546-bp tether, distal attachment geometry, at 0.5 mol/L NaCl. Dark markers: Dwell of low mobility. Light markers: High-mobility dwells. Black line: State trajectory from HMM analysis, indicating bound (lower level) and unbound state (upper level). (B and C) as in (A), but 1,554-bp and 2,562-bp tethers, respectively. (D) Mean bound vs. mean unbound dwell times per single-particle trajectory. Blue triangles: 546-bp tether. Orange circles: 1,554-bp tether. Purple squares: 2,562-bp tether. (E) Probability density histograms for dwell-times in the bound (Left column) and unbound state (Right column). Top to Bottom: 546-bp tether (blue), 1,554-bp tether (orange), and 2,562-bp tether (purple). Dashed lines: Truncated single-exponential probability densities from maximum-likelihood estimates. $\tau$'s: Inverse of the determined rate parameters. Errors: Statistical error from bootstrapping procedure ($\pm 3\sigma$). N's: Total numbers of dwell times pooled for the corresponding state and tether length. (F) On-rate (Left) and off-rate (Right) vs. tether length. Blue, orange, and purple markers as in (D). Gray markers: Data from 546-, 1,050-, 1,554-, 2,058-, and 2,562-bp tethers, proximal attachment geometry. Lines: Least-squares fits of the simplified model for influence of looping penalties on on-rate (Materials and Methods) to the data (Left), or mean value of all off-rates (Right).
lengths and using exemplarily an 8-bp-long DNA duplex with sequence CAGGAACG:CGTTCCTG (Fig. 4A–C). We do not observe a systematic effect of the concentration of sodium chloride on the rate of dissociation (Fig. 4D), beyond some slight variation in the measured dissociation rates. The factor between the fastest and slowest measured value was ∼1.4. The little differences we measure might be attributable to other external factors, such as slight temperature variations (on the order of 1°C) in our experiment. By contrast, increasing the concentration of sodium chloride had a strong effect on the rate of hybridization, causing up to fivefold acceleration upon an increase from 0.15 to 1 mol/L (Fig. 4E).

The tether length-dependent curves for binding rates as a function of salt concentration are parallel when plotting the observed variation in the measured dissociation rates. The factor between D chloride on the rate of dissociation (Fig. 4F) has negligible dependence on the salt concentration, while observe a systematic effect of the concentration of sodium sequence CAGGAACG:CGTTCCTG (Fig. 4G). We applied additive rates logarithmically (Fig. 4H). This behavior may be explained with an Arrhenius-like rate constant \( k_{\text{on}}(c, N) = A \cdot e^{-\Delta F(c) + g(N)/k_B T} \), where the activation barrier height is a sum of two terms \( f(c) \) and \( g(N) \), with the former being a function of the salt concentration \( c \) and the latter a function of the tether length \( N \). Hence,

\[
\ln(\kappa_{\text{on}}(c, N)) = \ln(A) + \frac{g(N)}{k_B T} - \frac{f(c)}{k_B T} + \text{offset}(N)
\]

The shape of our curves (Fig. 4I) is consistent with \( f(c) \sim \ln(c) \). From the kinetic rates for hybridization and dissociation, one may compute the equilibrium constant \( K_{\text{eq}} = k_{\text{on}}/k_{\text{off}} \). Since \( k_{\text{off}} \) has negligible dependence on the salt concentration, when \( \ln(k_{\text{on}}) \sim \ln(c) \), within the margin of error our data are in agreement with the empirical linear relationship of \( \ln(K_{\text{eq}}) \) vs. \( \ln(c_{\text{NaCl}}) \) derived by SantaLucia and Hicks (74) from ensemble duplex melting experiments in solution.

Hybridization Kinetics Depend Strongly on Sequence. We applied our system to study how the hybridization and dissociation kinetics of double-helical DNA domains vary with sequence. We designed a set of seven test sequences having virtually identical duplex free energy, according to the two-state nearest-neighbor model of DNA thermodynamic stability (74). The sequences had varying propensities to form secondary-structure motifs in the single strands of each designed duplex. We computed \( p_{\text{Hairpin}} \), the probability of at least one of the strands to reside in any secondary structure with stem length of at least two nucleotides, using free energies predicted by DNAmel/mfold (75) (Fig. 5A). The expectation is that the existence of such competing secondary structures affects the binding kinetics as seen in previous ensemble measurements (47, 49, 76). We performed a tethered-particle assay for each sequence variant, using the same tether length of 1,554 bp for all variants, in the presence of 0.5 mol/L NaCl. We collected fluorescence videos, extracted position–time traces for hundreds of single particles per variant, and determined the average dwell times in unbound and bound states for each analyzed particle. The resulting data were pooled to give the scatter plot shown in Fig. 5B. As expected, the sequence variants have quite different hybridization and dissociation kinetics. Whereas the fastest hybridizing variant 1 rapidly binds on the scale of 3 s, the slowest variant spends on average ∼500 s in the unbound state. Also, the duplex dissociation kinetics varies significantly, albeit less strongly than the hybridization kinetics. The average duplex lifetimes ranged from ∼5 s to ∼30 s depending on the variant. The spread in the scatter plot per variant reflects on the one hand the sample SD, which is equal to the ensemble mean value for a single-exponential probability density, and on the other hand the spread also reflects the number of transitions recorded per single particle (Fig. 5B, Insets). In particular, variant 7, which displayed extremely slow rebinding kinetics, underwent only a few transitions per recorded single-particle time trace. Hence, in this case, the average dwell times determined from a single-particle trace are statistically less well-defined compared with the other variants, causing the greater data point scatter for variant 7. As in our previous experiments with different tether lengths, the distribution of dwell times for the hybridized (Fig. 5C) and dissociated states (Fig. 5D), which we

![Fig. 4](image)

(A) Mean bound vs. mean unbound dwell times per single-particle trajectory at different concentrations of NaCl, as indicated by shade of markers. Duplex CAGGAACG:CGTTCCTG, 546-bp tether, distal attachment geometry. B and C as in A, but 1,554- and 2,562-bp tethers, respectively. (D) Off-rate vs. concentration of NaCl. Blue markers: 546-bp tether, orange markers: 1,554-bp tether, purple markers: 2,562-bp tether. Marker width: ±5% error in salt concentration due to pipetting errors and possible evaporation. Marker height: Statistical error from bootstrapping procedure (±2σ). Dashed lines: Mean value of the off-rates measured for the corresponding tether length. (E) As in D, but on-rates. Dashed lines: Linear fits to the values of \( \ln(k_{\text{on}}) \) vs. \( \ln(c_{\text{NaCl}}) \).
obtained by pooling all single-particle transition dwell times per variant, were virtually indistinguishable from single-exponential decays, for all variants analyzed herein.

Since the free energy of binding for all tested duplex variants was designed to be nearly identical, the ratio of the hybridization rate over dissociation rate should be a constant if one were to assume that secondary structures within the single strands do not occur. The ratio then gives the equilibrium constant $K_{eq}$, or the negative natural logarithm of the free energy difference between the unlooped and looped states of the system under study. Indeed, when plotting the obtained hybridization rates over the dissociation rate, we see a linear relationship for the variants with low $p_{Hairpin}$, that is, variants 1–4. However, the ratios of the kinetic rates obtained for the sequence variants 5–7 deviate significantly from the least-squares fit to the values from variants 1–4 (Fig. 5E).

As a first-order correction for the effect of secondary structures, we divided the measured on-rates by $1 - p_{Hairpin}$, the calculated probability for both strands to reside in a conformation free from hairpins with stem length of two or more nucleotides. For our 8-bp-long duplex sequences, this approach is very similar to applying the model published by Hata et al. (76), with the assumption that $\Delta_{seq} = 1$ for all nucleation sites. The correction yields an overall better agreement with a constant ratio of the kinetic rates (Fig. 5F and SI Appendix, Fig. S13), but variants 5 and 7 still deviate. Whereas there is only one possible hairpin structure in either strand of sequence variant 6, there are multiple possible secondary structures in the strands of variant 5 and 7.
7, which presumably will interchange rapidly. A description that considers only discrete states as we do in our calculation of $p_{\text{Hairpin}}$ may be overly simplified in such a case.

The $K_{eq}$ that we determined are approximately linearly related to the equilibrium constants $K_{eq}(\text{NN})$ predicted by the nearest-neighbor model (Fig. 5G), as expected (Materials and Methods). The slope of the linear fit puts the effective reactant concentration in our tethered-particle system at $\sim 9.8 \text{ nM}$. Given our tether length of 1,554 bp, this value is consistent with previous effective concentration estimations (77).

Full-Atom MD Simulations of Reversible Hybridization and Dissociation.
To help explain the molecular origin of the strong sequence dependence of the hybridization kinetics that we found experimentally, we used full-atom MD simulations, which were performed in a generalized Born-type implicit solvent (Materials and Methods and refs. 78 and 79). At 300 K, no reversible duplex formation could be observed during several microsecond simulation times. However, at elevated simulation temperatures (for the present simulation conditions: $\sim 340$–$350 \text{ K}$), it was possible to record multiple occurrences of reversible dissociation and rehybridization in single long-simulation trajectories (Fig. 6 B–D and Movie S2). When plotting the root-mean-square deviations (rmsd) of atom coordinates (heavy atoms) from the coordinates in standard B-DNA, time traces are obtained that reflect two-state like transitions, similar to the experimental data (Fig. 6 B–D). The simulations provide qualitative insight into the transition paths, as they reflect nucleation and subsequent fast propagation characterized by the initial formation of a short base pair contact and rapid zipper up to extend to the full duplex (Fig. 6 E–H). The propagation process occurs on a timescale of tens of nanoseconds after a successful initial nucleation, much faster than the time between successful encounters (Fig. 6 E–H). At the high simulation temperatures, no significant population of stable hairpin structures for the partner strands was observed. At lower simulation temperatures (e.g., 285 K, Fig. 6f) close to temperatures used in the experiments, the single-stranded partners of variants 6 and 7 sampled a high proportion of well-known GAGA tetraloop-like (80) and GCA triloop-like conformations (81) with one or two stem base pairs (Fig. 6f and Movie S3). Simulations of the single-stranded DNA partners indicate sequence-dependent tendencies of templating behavior: For example, in the case of sequence variant 1, which experimentally showed the highest hybridization rate, during the simulations the strand only containing purines frequently populates semihelical stacked conformations (Fig. 6 J and K). These offer a large exposed surface for initial binding of the partner strand, which raises the probability for forming a stable nucleus that promotes propagation rather than dissociation. Such tendency is also seen for fast-associating variant 2, and for variants 5 and 6. However, in the latter two cases, it is counteracted by the secondary structures in the dissociated single strands.

Fig. 6. Full-atom MD simulations. (A) Illustration of the reversible dsDNA formation and dissociation process for sequence variant 5 observed during MD simulations (stick model of DNA). (B–D) Root-mean-square deviation (rmsd) of heavy atoms (all nucleotides except terminal nucleotides) with respect to B-DNA vs. simulation time for simulations at 350 K (B), 345 K (C), and 340 K (D) (results shown for variant 5). An rmsd of $<3 \text{ Å}$ indicates double-strand formation except for possible fraying at the duplex termini. (E–H) Exemplary nucleation and propagation event of dsDNA formation: (E) rmsd vs. simulation time for the full duplex (variant 1). (F) Rmsd vs. simulation time of the fourth base pair step (a CCGG dsDNA), (G) rmsd of the neighboring fifth base pair step (a CT/GA step) forming $\sim 10 \text{ ns}$ after the first base pair step (indicated as vertical dotted lines). (H) Formation of the third base pair step. (I) Rmsd of sampled conformations with respect to hairpin reference structures (illustrated as stick models) from MD simulation of single strands at 285 K. (I, Top) Variant 6, strand AGCGAGT, which forms a well-known GNR-tetrapoop. (I, Bottom) Variant 7, strand AGCGAGTA, forming a central GCA-trilooop. Both hairpin structures include a characteristic sheared G/A loop-closing base pair. (J) Sequence-dependent tendency to form stacked single strands that adopt a structure close to B-form already in the absence of the partner strand, shown as probability distribution of rmsd with respect to a B-DNA reference, at elevated temperatures (2 µs at 345 K). Red/black solid lines: Fast-associating variant 1, strands GGAGGAGG and CCTCCTCC, respectively. Dotted lines: Both strands of variant 7. (K) Percentage of sampled stacked B-form-like single strands (in absence of binding partner) with rmsd relative to B-DNA $< 3 \text{ Å}$. Blue/yellow bars represent the first/second strand.
Discussion
In addition to establishing our assay, we saw that the concentration of monovalent ions has little influence on the duplex dissociation rates in the range from physiological concentration to 1 mol/L of NaCl. Our observations are consistent with the trends observed in previous single-molecule equilibrium FRET measurements with a 9-bp-long duplex (50), carried out in a lower salt regime from 5 to 50 mM NaCl, and with data from single-molecule confocal FRET measurements, albeit the authors describe a somewhat differing twofold decrease in the dissociation rate upon increasing the NaCl concentration from 0.1 to 1 mol/L (51). Our findings are also consistent with previous measurements from NMR and TLD (45) kinetic relaxation measurements after thermal jumps, which indicated salt concentration predominantly affects the association rates. However, in previous single-molecule FRET measurements with intramolecular DNA hairpin opening and closing, both reaction directions were affected by the salt concentration (82, 83), which raises the question of what causes the different behavior in the intramolecular (hairpin) vs. intermolecular hybridization.

Complementary to our experimental hybridization studies, we found that it is also possible to follow reversible duplex formation and dissociation in silico on the microsecond timescale, if we employ an implicit generalized Born solvent model, a reduced solvent viscosity, and elevated simulation temperatures compared with the experimental conditions. While a quantitative comparison with the experiments is not possible, the simulations provide qualitative insights on the order of the initial association and dissociation in silico on the microsecond timescale, if we find that it is also possible to follow reversible equilibrium binding kinetics of many other target systems beyond DNA duplexes. By taking advantage of molecular conjugation methods (84–87), protein–nucleic acid interactions, protein–protein interactions, and protein–ligand interactions could also be studied on the single-molecule level. For instance, to apply the assay to the study of a pair of interacting proteins, only two oligonucleotides need to be exchanged for the corresponding protein–DNA conjugates. For applications to protein–DNA interactions, one must consider that the tether may contain additional binding sites, which could interact with the protein under study. We expect that off-target binding with significant lifetime would manifest in the data as additional discrete states. Unwanted sequence motifs could be excluded a priori by modifying the scaffold strand. Similarly, users could also integrate multiple binding sites to perform competitive kinetic studies. In the future, it is also conceivable that multiple tethers and additional fluorescence dyes with different emission wavelengths may be integrated to study the sequence and kinetics of assembly of biomolecular complexes containing more than two reaction partners.

Materials and Methods
We used standard methods and chemicals for the design and preparation of our samples, which are described in SI Appendix, Materials and Methods. Instrumentation and procedures for data acquisition, as well as procedures and theoretical models for data analysis, are described in SI Appendix, Materials and Methods. The MD simulations are described in SI Appendix, Materials and Methods.

The authors declare that all data supporting the findings of this study are available within the paper, its supporting information files, or upon request from the authors.

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Correction

BIOPHYSICS AND COMPUTATIONAL BIOLOGY

Correction for “Tethered multifluorophore motion reveals equilibrium transition kinetics of single DNA double helices,” by Matthias Schickinger, Martin Zacharias, and Hendrik Dietz, which was first published July 23, 2018; 10.1073/pnas.1800585115 (Proc Natl Acad Sci USA 115:E7512–E7521).

The authors note that, due to a printer’s error, some of the text in the main article appeared incorrectly. On page E7518, right column, first full paragraph, line 7, “Δseq = 1” should instead appear as “δseq = 1.”

The authors also note that Table S4 in the SI Appendix appeared incorrectly. The SI Appendix has been corrected online.

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