On the formation of 2- and 3-cyanofurans and their protonated forms in interstellar medium conditions: quantum chemical evidence†

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The literature is still poor in theoretical and experimental, including both spectroscopic and thermodynamic data for protonated furan and protonated 2-cyanofuran and 3-cyanofuran (FH+, 2CFH+ and 3CFH+). These data are, however, crucial for astrophysicists and astrochemists in the detection of new species in interstellar medium (ISM), the discovery of these molecular species being not yet reported. It is in this perspective that a computational study based on quantum chemistry on FH+, 2CFH+ and 3CFH+ was undertaken. A series of properties including the proton affinity (PA) of furan and the two cyanofurans, the variations of enthalpy (ΔH), entropy (ΔS), and Gibbs free energy (ΔG) for the reactions yielding cyanofurans (neutral and protonated forms), were studied at different temperatures (5 K, 10 K, 150 K and 298 K) and pressures (P = 1 atm and P = 10−5 atm) based on modern computational models (G2MP2, G3, G4MP2 and G4). While confirming that the protonation favors the α-position for furan, the PA values show that the protonation favors the nitrogen atom in cases of 2CFH+ and 3CFH+. The ΔH, ΔS and ΔG values revealed spontaneous reactions producing these species under ISM conditions of temperature and pressure. In addition quadrupole hyperfine structures and vibrational spectra which are essential tools for the characterization and the identification of interstellar molecular species are predicted, while the region where brightest lines fall for different temperatures is discussed. The results reported in this work are expected to assist astrophysicists and astrochemists, in the search for new chemical species in interstellar environments.

1 Introduction

Despite unfavourable conditions to the chemical formation in the interstellar medium (ISM),1,2 more than a third of already detected molecules (more than 200 molecular species3) is made of complex organic molecules (COMs).4 In interstellar clouds and associated circumstellar envelopes of the asymptotic giant branch (AGB) stars, molecules with an order of magnitude of atom number ranging from 2 to 13 atoms in the gas phase have been discovered by high-resolution spectroscopy.5 Moreover, it has been argued that aromatic molecules and their protonated species as well as their substituted (heterocyclic) derivatives form an important component of the ISM.6,7 Furthermore, the discovery of some five- and six-membered molecular species in the dark molecular cloud TMC-1 and other ISM environments constitute a good evidence that aromatic chemistry is likely widespread in the earliest stages of star formation. This is, for instance, the discoveries of the benzenitrile,8 of the two cyanocyclopentadienes,9,10 that of the two cyanonaphthenes (1- and 2-cyanonaphthalenes),11 but also that of the indene (C9H8),12 the first pure polycyclic aromatic hydrocarbon (PAH) to be discovered in the ISM. The cyanobenzene has been also detected in prestellar regions,13 and tentatively in protostellar sources.14 These discoveries are also an evidence that organic molecules of high complexity are readily synthesized in regions with high visual extinction at remarkably low temperatures and pressures.
Early studies on the ISM molecular formation have revealed that ion-neutral reactions induced by cosmic rays are the primary reaction mechanism to form molecules in ISM shells and dense cloudy regions where temperatures are as low as 10 K. Moreover, the importance of grain surface formation is also reported in the literature. In general, among the three favorable environments to the molecular formation in space, i.e., the gas phase, the bare surface of dust and the mass of ice or its surface, the latter is suspected of being the seat of the formation of complex molecules. Complex organic species have been detected in hot nuclei within stars of high masses but also in regions called corinos where their formation takes place by the phenomenon of heating. Complex unsaturated molecular species are likely to be found in cold, dense regions such as the Taurus Molecular Cloud 1 (TMC-1, <10 K) where they, together with ions and radicals, are suggested to be formed on dust grains. Unsaturated complex species are also present in the so called lukewarm corinos L1527 (T > 30.00 K), which is known to contain significant abundances of complex molecules, including anionic forms. Of the detected molecules, a big part is found via rotational emission spectra, obtained through the use of millimeter wave telescopes on the ground or in space. A non-negligible part is also detected on the basis of vibrational transitions in the absorption infrared using background stars, whereas a small quantity is discovered by means of visible electron spectroscopy and UV rays against a star background through diffuse interstellar matter. Among the overall already detected molecules, only a very low proportion (≈2%) is of five- and six-membered types. They are, for instance, the four six-membered molecules, such as benzene (C6H6), its nitrile substituted derivative (benzonitrile: c-C6H5CN), and the two nitrile-group-functionalized PAHs (1- and 2-cyanonaphthalenes). For five-membered heterocyclic molecules, two molecular species have been reported: the highly polar cyano derivative of cyclopentadiene (c-C5H4CN), and the 2-cyanocyclopentadiene (C5H2CN)20. The high symmetry, and consequently, the lack of a permanent electric dipole moment of key aromatic building blocks like benzene and naphthalene (C6H5H) and also the five-membered heterocyclic compounds such as thiophene (C4H4S), furan (C4H4O)12 and pyrrole (C4H4NH) prevent their radio and millimeter detections. Nonetheless, a hydrogen-substitution with a cyano group (–CN) dramatically increases a molecule’s electric dipole moment relative to its non-substituted counterpart. It has been found a high abundance of oxygen and other elements in B stars and pointed. These authors have pointed out also that these young stars should most accurately model the abundance of oxygen. The literature search reveals that the atomic oxygen is depleted from interstellar gas at a rate that cannot even be explained. According to Lavoisier’s law, it may be reasonably hypothesized that the quantity of depleted oxygen would bind with other atoms to form new chemical species, which are not detected yet. In the same way, it has argued that the depletion of sulfur in regions where it is expected to be abundant may be explained by the detection of gas-phase sulfur-bearing molecules in which the sulfur should be bind with other atoms. Protonated species are known to play a key role in ion-molecule reactions in the gas phase interstellar chemistry. In fact, the H2+ ion plays a central role in interstellar chemistry, initiating chains of reactions which leads to the production of many complex molecular compounds observed in the interstellar medium (including protonated species) by neutral reactions. This ion was found to exist abundantly in various ISM environmental regions, especially, in dense molecular clouds, but also in diffuse clouds. Its abundance in the latter environment was found to be of orders of magnitude higher than in the former. Several protonated small molecules with a number of atoms ranging between 2 and 5 were found in the ISM. This is for instance the cases of H2COH+, O3H+, NCCNH+, C2H5+, etc. Up to know, only a few protonated complex organic molecules (COMs) have been detected in the ISM, even though it is established that they could evolve to the corresponding neutral species by dissociative recombination. For instance, the detections of CH2=CHCN+, HC=NH+, HCCN=CH+, C2NH+, etc., have been reported. Beside being of astrophysical importance, aromatic heterocyclic molecules have astrobiological relevance as precursors of nucleobases. A survey of the literature shows us very few reports on protonated heterocyclic compounds, especially, cyanofurans. Much effort has been focused on modelling the formation of small aromatic five- and six-membered rings and their subsequent reactions with smaller hydrocarbons and nitrogen species to produce PAHs and polycyclic aromatic nitrogen heterocycles. A recent theoretical work by Simbizi and coworkers on the protonation of thiophene, 2-cyanothiophene (2CT) and 3-cyanothiophene (3CT) under ISM conditions of temperature and pressure was carried out. To the best of our knowledge the hydrogenation of furan, 2-cyano furan and 3-cyano furan (Fig. 1) under the same conditions is not reported yet. The main objective of this investigation is to explore the formation of 2-cyano furan (2CF) and 3-cyano furan (3CF) and their protonated forms in the ISM conditions of temperature and pressure. The proton affinity (PA) of both 2CF and 3CF together with the enthalpy, entropy and Gibbs free energy changes (i.e., $\Delta H$, $\Delta S$ and $\Delta G$, respectively) of the reactions producing cyanofurans and the corresponding protonated forms are calculated at different conditions of temperature and pressure.

![Chemical structures of (a) furan, (b) 2-cyano furan (2CF) and (c) 3-cyano furan (3CF): 1 to 7 are different positions of protonation.](image_url)
pressure and with the aid of modern quantum chemical methods. The structures of protonated cyanofurans (C₆H₅O–CFNH⁺) are characterized through their vibrational and rotational spectra.

2 Computational details

Density functional theory (DFT) calculations were performed with the aid of Gaussian 09 package. The G09 package was used to build the starting molecular structures. Geometrical parameters for furan, 2CFH⁺, 3CFH⁺ and HCNH⁺ are determined using the method described and used in previous works. This methodology includes geometry optimization followed by empirical corrections for systematic deficiencies of methods and basis sets and adjustments to some geometrical parameters. Based on this method, the B3LYP/6-31G(d,p) level of theory was chosen. This optimization scheme is first applied on furan which has experimental data and thereafter applied to 2CF, 3CF and their protonated forms (2CFH⁺, 3CFH⁺, respectively). Thermodynamic properties including the proton affinity, the entropy, enthalpy and Gibbs free energy changes (ΔrS, ΔrH and ΔrG in kJ mol⁻¹) for reactions producing the cyanofurans and their protonated forms are calculated at G2MP2 and G3. The calculations of these properties were done under different conditions of temperature (T = 298 K, T = 150 K, T = 10 K and T = 5 K) and pressure (P = 1 atm and P = 10⁻⁵ atm) prevailing in ISM environments where the present protonated species or COMs, in general, are expected to be found. These two levels were chosen because they give results which are close to the experimental value for existing furan. To improve the accuracy of the thermodynamic properties, these quantities were recomputed using the G4 and G4MP2 methods. The harmonic frequencies for RCNH⁺ were calculated at B3LYP/6-31G(d,p) level of theory. The optimized geometric structures from the literature were considered. The results reveal a very good agreement between calculated and experimental structures. Geometrical parameters for furan and HCNH⁺. Indeed, recalling that rotational constants are extremely linked to the molecular structure through the moment of inertia components, the comparison of calculated and experimental rotational constants in Table 2 for furan reveals a very good agreement between them. This agreement supports the accuracy of the used method and the reliability of the calculated results. Thus, applying the same methodology is reasonably to lead to accurate structures for both the neutral (2CF and 3CF) and the protonated (2CFH⁺ and 3CFH⁺) species forms for which no experimental data are reported yet. As expected, the comparison of calculated and experimental rotational constants in Table 2 for furan reveals a very good agreement between them. This agreement is also an evidence that the calculated structures for all the molecular species are reliable and close to the experimental ones. The optimized 3D molecular geometries are displayed in Fig. 2 and S1. It should be noted that HCNH⁺ is a linear molecule belonging to the Cᵥ point group. While the inertial defect values (ΔI in Table 2) for furan, 2CF, 3CF and 3CFH⁺ are ≈0 (i.e., 0.000, 0.001 and −0.001 amu Å², respectively), indicating that they are totally planar, those for 2CFH⁺ and 3CFH⁺ being high (≈0.306 and 0.309 amu Å²) indicating that these forms are distorted and non planar. The N–H is bent out of the plan containing the remaining atoms; the hydrogen atom is thus out of

Table 1: RMSD bond length (in Å), bond angles (in °) and rotational constants (in MHz) for furan for at different assessed levels of theory with respect to experimental results.

| Level of theory | Bond lengths/Exp° | Bond angles/Exp° | Rotational constants/Exp° |
|----------------|-------------------|-----------------|--------------------------|
| HF/6-31G(d)    | 0.0154            | 0.3817          | 246.4136                 |
| MP2/6-31G(d,p) | 0.0034            | 0.2449          | 44.9147                  |
| MP3/6-311G(d)  | 0.0052            | 0.2204          | 39.9478                  |
| M06-2X/6-31G(d,p) | 0.0051          | 0.1852          | 91.3475                  |
| M06-2X/6-311G(2d,2p) | 0.0068       | 0.2449          | 134.6708                 |
| B3LYP/6-31G(d) | 0.0036            | 0.3780          | 10.4848                  |
| B3LYP/6-31G(d,p) | 0.0031          | 0.2976          | 11.6142                  |
| B3LYP/6-311G(2d,2p) | 0.0033        | 0.2976          | 67.2463                  |
| B3LYP/6-311+G(2d,2p) | 0.0031       | 0.2928          | 60.7535                  |
| B3LYP/6-31+G(d)  | 0.0043            | 0.3338          | 14.7672                  |
| B3LYP/6-311G(2df,2p) | 0.0075       | 0.2070          | 147.9445                 |
| B3LYP/6-31G(d,p)  | 0.0078            | 0.6164          | 1.3454                   |

° Experimental data from Bak et al. (1962). Calculated at B3LYP/6-31G(d,p) + empirical correction.

3 Results and discussion

3.1 Geometrical parameters

Experimental and calculated bond lengths (in Å), bond angles (in °) and rotational constants (in MHz), as well as deviations with respect to experimental rotational constants at different levels of theory are presented in Table S1 in the ESIF file. Table 1 contains root mean square deviations (RMSD) for bond length (in Å), bond angles (in °) and rotational constants (in MHz) for furan for the different assessed levels of theory with respect to experimental results. As shown by the results in this table, for a given method, the larger is the basis set the higher is the accuracy for the geometrical structure. However, the accuracy of the rotational constants which are strongly linked to the molecular structure does not follow this increase of basis set. A careful analysis of the results in Table 1 reveals that B3LYP/6-31G(d) and B3LYP/6-31G(d,p) reproduce, relatively well the geometric structure, but also very well the rotational constants for furan compared with other levels of theory. B3LYP/6-31G(d,p) was therefore chosen for the empirical correction as it combines the geometrical structure accuracy as well that of the rotational constants. The optimized geometric structures (including empirical corrections) at B3LYP/6-31G(d,p) for furan, 2CF, 3CF, 2CFH⁺ and 3CFH⁺ are presented in Tables 2 and S2. For calibration of the method, the protonated form of cyanide (HCNH⁺ see Fig. S1) for which experimental structure is known from the literature was considered. The results reveal a very good agreement between calculated and experimental structures for furan and HCNH⁺. Indeed, recalling that rotational constants are extremely linked to the molecular structure through the moment of inertia components, the comparison of calculated and experimental rotational constants in Table 2 for furan reveals a very good agreement between them. This agreement supports the accuracy of the used method and the reliability of the calculated results. Thus, applying the same methodology is reasonably to lead to accurate structures for both the neutral (2CF and 3CF) and the protonated (2CFH⁺ and 3CFH⁺) species forms for which no experimental data are reported yet. As expected, the comparison of calculated and experimental rotational constants in Table 2 for 2CF reveals also a very good agreement between them. This agreement is also an evidence that the calculated structures for all the molecular species are reliable and close to the experimental ones. The optimized 3D molecular geometries are displayed in Fig. 2 and S1.
3CFH⁺ (bond lengths in Å, bond angles in °), rotational constants in MHz, principle moments of inertia and the inertial defects in amu Å².

### Table 2

| Bond length | Furan | 2CF | 3CF | 2CFH⁺ | 3CFH⁺ |
|-------------|-------|-----|-----|-------|-------|
| O–C2       | 1.358  | 1.362 |      | 1.358 | 1.422 |
| O–C5       | 1.358  | 1.362 |      | 1.350 | 1.365 |
| C2–C3      | 1.362  | 1.361 |      | 1.367 | 1.374 |
| C3–C4      | 1.452  | 1.431 |      | 1.446 | 1.441 |
| C4–C5      | 1.362  | 1.361 |      | 1.373 | 1.347 |
| C2/C3–C6   | —     | —    |      | 1.099 | 1.416 |
| C≡N        | —     | —    |      | 1.171 | 1.165 |
| N–H        | —     | —    |      | —     | 1.011 |

### Bond angle

| C5–O–C2    | 107.13 | 106.5 | 105.42 | 107.35 | 105.60 |
| O–C2–C3    | 110.814| 110.7 | 112.29 | 110.41 | 111.64 |
| O–C5–C4    | 110.814| 110.7 | 113.28 | 110.85 | 111.99 |
| C5–C4–C3   | 105.622| 106.0 | 103.52 | 105.96 | 105.89 |
| C2–C3–C4   | 105.622| 106.0 | 105.66 | 105.43 | 104.87 |
| C2/C3–C6=N | —     | —    | —     | 179.54 | 175.05 |
| C6=N–H     | —     | —    | —     | 155.00 | 179.87 |

| Constantes rotationnelles |
|---------------------------|
| A | 9446.06 | 9446.94 | 9220.097 | 9220.106 | 9374.251 | 9070.367 |
| B | 9246.25 | 9246.64 | 2028.751 | 2029.262 | 1936.447 | 1924.174 |
| C | 4672.54 | 4670.85 | 1662.861 | 1662.640 | 1604.917 | 1588.967 |

### Principal moments of inertia and inertial defect

- $I_a$ (amu Å²): 191.051 - 195.727 - 53.911 - 55.715 - 55.717
- $I_b$ (amu Å²): 195.194 - 889.394 - 260.983 - 262.653 - 262.647
- $I_c$ (amu Å²): 386.245 - 1085.120 - 314.895 - 318.062 - 318.055
- $\Delta I$ (amu Å²): 0.000 - 0.001 - 0.001 - 0.306 - 0.309

* Numbering scheme used is that of Fig. 1 and Scheme S1. b Experimental data from Bak et al. 44 Experimental data from Engelbrecht & Sutter. 44

3.2 Sites of protonation

The protonation (or hydrogenation) is the addition of a proton (H⁺) to an atom, or molecule, forming the conjugate acid according to eqn (1).

$$ A + H⁺ \rightarrow AH^+ $$

The proton affinity (PA) of a chemical species A is the negative of the change in enthalpy associated with the gas phase protonation of the reaction.\(^{25}\) The PA is defined by enthalpy changes in eqn (2):

$$ PA = \Delta H(A) + \Delta H(H⁺) - \Delta H(AH⁺) \tag{2} $$

where $\Delta H(A)$ and $\Delta H(AH⁺)$ are enthalpies of the unprotonated and protonated compound, respectively.

The PA of furan was calculated at different positions using G2MP2 and G3 at different temperatures (298 K, 150 K, 10 K and 5 K for $P = 1$ atm). The results are presented in Table 3. These temperatures are in the range of temperatures prevailing in molecular clouds where complex organic molecules (COMs) are expected to be found (10–300 K).\(^{31,52}\)

The protonation site for C₄H₄O and C₄H₅N has been investigated by resonant infrared multiphoton dissociation (IRMPD) spectroscopy in the 900–1700 cm⁻¹ range employing the free electron laser (FEL) at the Centre Laser Infrarouge Orsay (CLIO) by Ulrich and his coworkers.\(^{44}\) B3LYP/6-311G(2df,2pd) level of theory has demonstrated that only the C₄ protonated isomers are observed, and corresponds to the global minima on the potential energy surfaces. These results show that C₄ is the preferred site of protonation. The National Institute of Science and Technology (NIST) provides also a value for the PA of furan, i.e., $PA = 812$ kJ mol⁻¹.\(^{31}\) This later value was calculated using Fourier transform ion cyclotron resonance (FT-ICR) mass spectrometry. Small discrepancies are observed then between this value and the results in Table 3: $\delta = 3.91$ kJ mol⁻¹ for G2MP2 and $\delta = 2.80$ kJ mol⁻¹ for G3 at 298 K; $\delta = 1.46$ kJ mol⁻¹ for G2MP2 and $\delta = 0.35$ kJ mol⁻¹ for G3 at 150 K; and $\delta = 1.28$ kJ mol⁻¹ for G2MP2 and $\delta = 2.39$ kJ mol⁻¹ for G3 at 10 K. The comparison of these results with the value of NIST shows...
with G2MP2 and G3 at $T = 298$ K and $T = 10$ K are shown in Tables 4 and S3,\textsuperscript{†} whereas those calculated at $T = 150$ K and $T = 5$ K are presented in Table S4.\textsuperscript{†} According to the PA values, the favorable protonation site is the nitrogen atom for both the 2CF and 3CF at considered temperatures (see Tables S3 and S4 for details). The results show us again that upon the protonation of the furan ring in the ISM conditions of temperature and pressure, the $a$-position is the most favorable site. A comparison between $a$ and $b$ protonation either for 2CF or 3CF shows that it occurs in $a$-position for both 2CF and 3CF. The PAs for these compounds in the decreasing order are such that $PA(a) < PA(b) < PA(c)$. Considering that the site with high $a$-position for the proton corresponds to the site which has a high probability of attack by the proton,\textsuperscript{26} the results show that the $a$-position is the most favorable site for protonation of furan, confirming the existing literature.\textsuperscript{25}

The PA is also calculated for the nitrile substituted derivatives (2CF and 3CF) for the same temperatures ($298$ K, $150$ K, $10$ K and $5$ K) for the pressure ($P = 1$ atm). The results calculated a good agreement at $150$ K, especially with G3 when the protonation is performed at the $C_a$. The calculated proton affinities for furan in the ascending order are such that $PA(O) < PA(b) < PA(a)$. Considering that the site with high $a$-position for the proton corresponds to the site which has a high probability of attack by the proton,\textsuperscript{26} the results show that the $a$-position is the most favorable site for protonation of furan, confirming the existing literature.\textsuperscript{25}

The results reveal that the $\Delta_H$, $\Delta_S$ and $\Delta_G$ for the reactions leading to the formation of 2CF/3CF and their protonated forms are spontaneous.\textsuperscript{26} It is worthy noting that these quantities are also negative regardless the used method. These results imply that all reactions are spontaneous at the considered conditions of temperature and pressure, conditions prevailing in ISM regions where COMs are mostly detected. They also imply that cyanofurans and their protonated forms are likely to be produced barrierlessly via the proposed reactions.

### 3.3 Enthalpy ($\Delta_H$), Gibbs free energy ($\Delta_G$) and entropy ($\Delta_S$) changes of the reactions producing 2CF/3CF and their protonated forms

The reactions yielding R–CN/R-CN$^+$ and the corresponding enthalpy ($\Delta_H$), entropy ($\Delta_S$) and Gibbs free energy ($\Delta_G$) changes are explored using G2MP2 and G3 at different temperatures ($298$ K, $150$ K, $10$ K and $5$ K) and low pressure ($P = 10^{-5}$ atm). Calculations using G4MP2 and G4 were also performed at $298$ K and $10$ K and low pressure ($P = 10^{-5}$ atm). The results for G2MP2, G3, G4MP2 and G4 for $T = 298$ K and $T = 10$ K are shown in Table 5, whereas those for G2MP2 and G4 at $T = 150$ K and $T = 5$ K are presented in Table S5.\textsuperscript{†}

The results for $\Delta_H$, $\Delta_S$ and $\Delta_G$ are all negative, implying that the reactions leading to the formation of 2CF/3CF and their protonated forms are spontaneous.\textsuperscript{26} It is worthy noting that these quantities are also negative regardless the used method. These results imply that all reactions are spontaneous at the considered conditions of temperature and pressure, conditions prevailing in ISM regions where COMs are mostly detected. They also imply that cyanofurans and their protonated forms are likely to be produced barrierlessly via the proposed reactions.

### Table 3 G2MP2 and G3 proton affinity (PA in kJ mol$^{-1}$) of furan at different sites of protonation and temperatures ($T = 298$ K, $T = 150$ K, $T = 10$ K and $T = 5$ K)

| Sites of protonation | Method | $O$ | $C_a^a$ | $C_b^b$ | $O$ | $C_a^a$ | $C_b^b$ |
|---------------------|--------|-----|--------|--------|-----|--------|--------|
|                     |        |     |        |        |     |        |        |
|                     |        |     |        |        | 298 K |        |        |
|                     |        |     |        |        | 298 K | 815.91 | 771.73 |
|                     |        |     |        |        |    G2MP2 | 701.41 | 814.80 |
|                     |        |     |        |        |    G3 | 697.78 | 719.69 |
|                     |        |     |        |        | 150 K |        |        |
|                     |        |     |        |        | 150 K | 813.46 | 769.54 |
|                     |        |     |        |        |    G2MP2 | 701.41 | 814.80 |
|                     |        |     |        |        |    G3 | 697.78 | 719.69 |
|                     |        |     |        |        | 10 K |        |        |
|                     |        |     |        |        | 10 K | 810.72 | 766.83 |
|                     |        |     |        |        |    G2MP2 | 696.07 | 809.61 |
|                     |        |     |        |        |    G3 | 693.19 | 763.28 |
|                     |        |     |        |        | 5 K |        |        |
|                     |        |     |        |        | 5 K | 810.62 | 766.73 |
|                     |        |     |        |        |    G2MP2 | 696.07 | 809.61 |
|                     |        |     |        |        |    G3 | 693.19 | 763.28 |
|                     | NIST   | 812$^c$ |        |        | 812$^c$ |        |        |

$^a$ $C_a$ and $C_b$ are atoms number 2 ($a$-position) and 3 ($b$-position) on Fig. 1; $^c$ Experimental data from Van et al.\textsuperscript{31} (NIST).
3.4 Vibrational parameters of 2CFH⁺ and 3CFH⁺

The use of IR spectroscopy is a reliable mean in the identification of chemical species in ISM.51,52 However, the IR spectra are not reported yet for the 2CFH⁺ and 3CFH⁺ species. In this study, the simulation of vibrational spectra for the protonated cyano-furans, supported by the potential energy distribution (PED) is performed. The vibrational and rotational spectra for non protonated forms are dealt in another works.

During the PED analysis, the contribution of each vibrational mode as well as the atoms involved for the 27 vibrational modes are distributed in the two representations of symmetry of the point group C₂: 3N - 6 = 204 (in-plan modes) + 7A² (out-of-plan modes) for 2CFH⁺ and C₂: 3N - 6 = 184 (in-plan modes) + 9A³ (out-of-plan modes) for 3CFH⁺ as shown in the Tables S6 and S7.† The NH and CH stretching modes for the species studied are characterized in the region where they are supposed to appear, i.e., in the range 3000–3800 cm⁻¹.53,54 In fact, the NH stretching modes appear at 3475 and 3486 cm⁻¹ for 2CFH⁺ and 3CFH⁺, respectively, with PED = 97% for both these compounds. Likewise, the CH stretching modes appear at 3176, 3130 and 3122 cm⁻¹ with contributions of 97, 98% and 98%, respectively, for 2CFH⁺. These modes of vibrations appear also at 3147, 3120 and 3120 cm⁻¹ with contributions of 98%, 99% and 99%, respectively, for 3CFH⁺. The analysis of results in Table S8† shows that, whereas the lines corresponding to NH are very strong in IR for both compounds (* ≈ 1034 km mol⁻¹ for 2CFH⁺ and 1135 km mol⁻¹ for 3CFH⁺), those corresponding to CH are relatively weak (* ≈ 20 km mol⁻¹ for the most intense for 2CFH⁺ and * ≈ 24 km mol⁻¹ for the most intense for 3CFH⁺). It is worthy stating that, from the results in this table, the Raman lines in this region are weak for both the two molecular species. Moreover, from the calculated frequencies and modes presented in Tables S6 and S7,† the in-planes and out-of-plane deformations characterizing the protonation, i.e., the one involving NH, have significant contributions below 650 cm⁻¹. Indeed, the in-plane deformations contribute at 590 cm⁻¹ (PED = 15%), 575 cm⁻¹ (PED = 20% and at 279 cm⁻¹ (PED = 62%) for 2CFH⁺. They contribute at 592 cm⁻¹ (PED =

### Table 4  
G2MP2 and G3 proton affinity (PA in kJ mol⁻¹) of 2CF and 3CNF at different sites of protonation and temperatures (T = 298 K and T = 10 K)

| Sites | G2MP2 (in-plan modes) | G3 (in-plan modes) | G2MP2 (out-of-plan modes) | G3 (out-of-plan modes) |
|-------|----------------------|--------------------|---------------------------|------------------------|
| 1     | 643.39 (635.93)      | 642.18 (634.71)    | 636.48 (631.33)           | 635.54 (630.39)        |
| 2     | 732.07 (726.97)      | 727.39 (722.29)    | 753.58 (746.65)           | 751.89 (746.96)        |
| 3     | 702.78 (698.23)      | 701.18 (696.65)    | 677.78 (672.97)           | 672.71 (667.90)        |
| 4     | 709.78 (705.07)      | 707.45 (702.76)    | 709.00 (704.26)           | 706.34 (701.60)        |
| 5     | 747.83 (742.97)      | 746.38 (735.37)    | 747.75 (742.78)           | 745.32 (740.35)        |
| N     | 795.14 (790.48)      | 796.35 (791.69)    | 801.47 (796.57)           | 802.75 (797.85)        |

* Position numbering scheme is from Fig. 1 and Scheme S1.

### Table 5  
Gase phase G2MP2, G3, G4MP2 and G4 calculated enthalpy, entropy and Gibbs free energy variations (ΔH, ΔS and ΔG in kJ mol⁻¹) of reaction producing cyano-furans and their protonated forms (T = 298 K and T = 10 K for P = 10⁻¹ atm)

| Reactions | No | ΔHₐ | ΔS | ΔGₐ | Method |
|-----------|----|-----|----|-----|--------|
| CH₃CN⁻ + H⁺ → 2CF + H⁺ | (1) | -532.03 | -517.07 | -0.050 | -532.08 | -533.44 | -0.045 | G2MP2 |
| C₂H₄CN⁻ + H⁺ → 3CF + H⁺ | (2) | -567.38 | -552.65 | -0.050 | -568.98 | -568.54 | -0.044 | G3 |
| C₂H₄CN⁻ + H⁺ → 3CF + H⁺ | (3) | -556.02 | -541.13 | -0.050 | -557.54 | -557.09 | -0.045 | G4MP2 |
| C₂H₄OCN + H₂ → 2CFH⁺ + H₂ | (4) | -561.53 | -546.64 | -0.050 | -563.05 | -562.61 | -0.045 | G3 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (5) | -538.90 | -523.98 | -0.050 | -539.84 | -540.29 | -0.044 | G4MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (6) | -573.73 | -558.84 | -0.049 | -574.67 | -578.11 | -0.043 | G3 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (7) | -563.38 | -548.60 | -0.050 | -564.93 | -564.49 | -0.045 | G4MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (8) | -568.66 | -553.88 | -0.050 | -570.21 | -569.77 | -0.045 | G4 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (9) | -374.98 | -369.79 | -0.017 | -375.31 | -373.49 | -0.182 | G2MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (10) | -375.89 | -370.63 | -0.017 | -376.00 | -375.89 | -0.010 | G3 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (11) | -372.72 | -365.70 | -0.024 | -371.85 | -371.73 | -0.011 | G4MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (12) | -373.42 | -363.75 | -0.045 | -372.54 | -372.43 | -0.012 | G4 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (13) | -381.31 | -375.59 | -0.019 | -381.49 | -379.58 | -0.019 | G2MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (14) | -382.28 | -376.56 | -0.019 | -382.18 | -382.07 | -0.010 | G3 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (15) | -377.74 | -372.88 | -0.024 | -378.16 | -378.04 | -0.012 | G4MP2 |
| C₂H₄OCN + H₂ → 3CFH⁺ | (16) | -378.28 | -373.42 | -0.016 | -378.69 | -377.29 | -0.139 | G4 |
59%) and at 168 cm$^{-1}$ (PED = 47%) for 3CFH$^+$. Similarly, the out-of-plane deformation modes contribute at 630 cm$^{-1}$ (PED = 23%), 542 cm$^{-1}$ (PED = 78%) and at 179 cm$^{-1}$ (PED = 23%) for 2CFH$^+$. They contribute also at 628 cm$^{-1}$ (PED = 35%), 627 cm$^{-1}$ (PED = 91%), 489 cm$^{-1}$ (PED = 21%) and at 209 cm$^{-1}$ (PED = 68%) for 3CFH$^+$. The in-plane CH deformations appear in the range 872–1546 cm$^{-1}$ with high contributions at 1190 cm$^{-1}$ (PED = 75%) for 2CFH$^+$ and in the range 755–1591 cm$^{-1}$ with high contributions at 1222 cm$^{-1}$ (PED = 83%) and at 1099 cm$^{-1}$ (PED = 76%). In the same way, the out-of-plane CH deformations appear in the range 179–875 cm$^{-1}$ with main contributions at 875 cm$^{-1}$ (PED = 86%), at 839 cm$^{-1}$ and 875 cm$^{-1}$ with PED = 88% for 2CFH$^+$. For 3CFH$^+$, these vibrations modes appear in the range 209–887 cm$^{-1}$, contributing mainly at 889 cm$^{-1}$ (PED = 94%), 882 cm$^{-1}$ (PED = 88%), and at 808 cm$^{-1}$ (PED = 89%). IR and Raman intensities for protonated forms (2CFH$^+$ and 3CFH$^+$) are presented in Table S8† and plotted in Fig. S2 and S3.†

3.5 Rotational parameters of 2CFH$^+$ and 3CFH$^+$

The calculated rotational parameters for the two protonated species (in addition to those related to the molecular geometry presented in Table 2) are provided in Table 6. In general, protonation spectroscopic data are of great importance in unambiguously identifying the protonated species in the ISM. In particular, hyperfine spectra, besides identifying the protonation site(s), also unravel the structural attribution of various isomers. The present work is the first study on the rotational spectroscopic properties of 2CFH$^+$ and 3CFH$^+$. The rotational parameters play an important role in the characterization of the spectra of molecules. A molecule has a spectrum if it has a permanent dipole moment. For the first times, rotational constants of protonated cyanofuranos are provided. The results summarized in Table 6 show that 2CFH$^+$ has a small dipole moment compared 3CFH$^+$. Protonated hydrogen cyanide is a case of protonated simple molecular species which has drawn much attention because of its importance in the chemistry of interstellar clouds. It had been searched in many different environmental media and was, first, detected very early towards Sgr B2$^+$ through three pure rotational transitions 1–0, 2–1 and 3–2 at 74, 148 and 222 GHz, respectively. It was, later, found in dark clouds towards TMC-1 (T = 10 K) through the quadrupole hyperfine structure of 1–0 and in the DR 21(OH) compact H II region. It had even been detected in L1544 (T = 7 K). For non protonated forms, only 2CF has experimental rotational constants (Table 2). Results in this table show a very good agreement between experimental and calculated values for this molecule (ΔA = 0.009, ΔB = 0.5512 and ΔC = 0.221 MHz). We therefore expect the same accuracy for molecular species without experimental results, including protonated cyanofuranos. Fig. 3 presents simulated rotational spectra (including $^{14}$N hyperfine quadrupole couplings) for 2CFH$^+$ and 3CFH$^+$ at $T = 7$, 10, 30, 100, 150 K and 300 K. The analysis of these spectra reveals that the most intense lines are observed for low temperatures. Indeed, temperatures (T = 7 K and T = 10 K), i.e., the temperature prevailing in TMC-1 or in many cold molecular clouds known to host COMs. The presence of the $^{14}$N quadrupole nucleus induces lines splittings. Indeed, Tables S9 and S10 show the B3LYP/6-31G(d,p) calculated strongest quadrupole hyperfine structure for 2CFH$^+$ and 3CFH$^+$, respectively, at $T = 10$ K. The results in these tables confirm, as it has been found from the Fig. 3, that the brightest lines are in the regions of frequencies around 45 GHz. For instance, Table S9 shows that the three strongest transition lines are $13_1_{12} \leftrightarrow 12_1_{11}$, $12_1_{11} \leftrightarrow 11_1_{10}$ and $13_0_{13} \leftrightarrow 12_0_{12}$ centered at $\sim 46$ 479, $\sim 43$ 124.5 MHz and $\sim 45$ 054 MHz, respectively. Likewise, the analysis of results in Table S9 reveals also that the three strongest transition lines are $13_1_{12} \leftrightarrow 12_1_{11}$, $12_1_{11} \leftrightarrow 11_1_{10}$ and $14_0_{14} \leftrightarrow 13_0_{13}$ centered in the regions around $\sim 45$ 438, $\sim 42$ 142 MHz and $\sim 45$ 216 MHz, respectively. A common analysis of results in these two tables reveals that the strongest component for a $J_{K_x,K_z} \leftrightarrow J_{K_x,K_z} + 1$ transition correspond to the term for which $F'' = J' + 1$ and $F'' = J' + 1$. It is followed by the component corresponding to $F'' = J' \leftrightarrow F = J'$. Then that corresponding to $F'' = (J' - 1) \leftrightarrow F = (J' - 1)$. Terms corresponding to $F'' = (J' - 1) \leftrightarrow F = (J' - 1)$ are weak with equal intensities, whereas $F'' = (J' - 1) \leftrightarrow F = (J' + 1)$ is the weakest one, with intensity nearly equal to zero. These observations are common either for 2CFH$^+$ or 3CFH$^+$. For both the two molecular species, strong lines correspond to the values of J in the range 11–15. Moreover, the analysis of Fig. 3 and Tables S9, S10 reveals also that transitions lines are stronger for 3CFH$^+$ than for 2CFH$^+$. Indeed, the 3CFH$^+$ strongest line is about five times stronger than the 2CFH$^+$ strongest line. For instance, the 3CFH$^+$ line $13_{13} \leftrightarrow 14 \leftrightarrow 12_{11}$, 13 at 45 483.0092 MHz has intensity of 46.4430 $\times 10^{-3}$ mm$^2$ MHz, whereas, $13_{13} \leftrightarrow 14 \leftrightarrow 12_{11}$, 12 appearing at 46 479.2457 MHz has intensity of 8.7264 $\times 10^{-3}$ mm$^2$ MHz. In other words, one may find that the rotational spectrum for 2CFH$^+$ is less intense than that for 3CFH$^+$. The rotational line intensity being proportional to the square of the dipole moment, this disparity in line intensity for the

| Rotational parameters | 2CFH$^+$ | 3CFH$^+$ |
|-----------------------|----------|----------|
| $\Delta_0$ (kHz)      | 0.068    | 0.081    |
| $\Delta_1$ (kHz)      | 1.002    | 12.379   |
| $\Delta_2$ (kHz)      | 2.185    | 1.901    |
| $\Delta_3$ (kHz)      | 0.012    | 0.109    |
| $\Delta_4$ (kHz)      | 1.276    | 1.107    |
| $\mu_\alpha$ (debye)  | 3.151    | 5.417    |
| $\mu_\beta$ (debye)   | 1.118    | 0.045    |
| $\mu_\gamma$ (debye)  | 1.126    | 0.380    |
| $\mu_{\alpha\alpha}$ (debye) | 3.970 | 5.430 |
| $\alpha_\alpha$ (MHz) | 1.028    | 1.247    |
| $\alpha_\beta$ (MHz)  | 0.955    | 0.347    |
| $\alpha_\gamma$ (MHz) | -1.983   | -1.595   |
| $\kappa$              | -0.910   | -0.918   |
rotational spectra of these two species is ascribable to the difference in their dipole moments (see Table 6).

4 Conclusions

For the first time, the thermodynamics of reactions leading to the formation of furan, 2-cyanofuran, 3-cyanofuran and their protonated forms under interstellar (ISM) conditions of pressure (1 atm and 10⁻⁵ atm) and temperature (5 K, 10 K, 150 K and 298 K) was conducted. The predicted enthalpy change ($\Delta H$), the entropy change ($\Delta S$) and the Gibbs free energy change ($\Delta G$) of reactions, with the aid high performance methods (G3, G2MP2, G4 and G4MP2) has shown that all these thermodynamic properties have negative values under ISM conditions of pressure and temperature. Accordingly, it was concluded that these heterocyclic molecules emerge spontaneously in this medium.

In addition, geometrical structures, vibrational an rotational spectra of the protonated species were investigated. IR lines corresponding to the NH stretching modes (characteristic of the protonation) were found to be very strong whereas, the Raman lines were found to be weak. From rotational analysis at temperature prevailing in molecular clouds where COMs are expected to be discovered ($T \approx 10$ K, stronger lines are located in the regions around 45 GHz for both 2CFH⁺ and 3CFH⁺. Rotational lines (or strong hyperfine structure components) were found to be more intense in 3CFH⁺ than 2CFH⁺. In a context of gap in the scientific knowledge about these species, we believe that these data will serve for astrophysical and astrochemical purposes in detection of new entities in interstellar medium.

Conflicts of interest

No conflict of interest to declare.

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