Nonlinear analog spintronics with van der Waals heterostructures

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The current generation of state-of-the-art spintronic devices, which use electron-spin relies on linear operations for spin-injection, transport and detection processes. The existence of nonlinearity in a spintronic device is indispensable for spin-based complex signal processing operations. Here we for the first time demonstrate the presence of electron-spin dependent nonlinearity in a spintronic device, and measure up to 4th harmonic spin-signals via nonlocal spin-valve and Hanle spin-precession measurements. We demonstrate its application for analog signal processing over pure spin-signals such as amplitude modulation and heterodyne detection operations which require nonlinearity as an essential element. Furthermore, we show that the presence of nonlinearity in the spin-signal has an amplifying effect on the energy-dependent conductivity induced nonlinear spin-to-charge conversion effect. The interaction of the two spin-dependent nonlinear effects in the spin transport channel leads to a highly efficient detection of the spin-signal without using ferromagnets. These effects are measured both at 4K and room temperature, and are suitable for their applications as nonlinear circuit elements in the fields of advanced-spintronics and spin-based neuromorphic computing.

Nonlinear elements, such as transistors and diodes, led Shockley and coworkers [1] to lay the foundation for electronics revolution, and underlie the modern-day electronics. However, such elements lack in the field of spintronics. Major ideas in the field of spintronics thus far have suggested the possibility of achieving a gate operation requiring nonlinearity can not be executed. Interestingly, the differential spin-injection efficiency $p_{\text{inj}}$ of ferromagnetic (FM) tunnel contacts with atomically flat and pinhole-free thin hBN flakes as a tunnel barrier [12, 13] depends on the input dc bias current $I$ [1, 15, 16], and renders them as a viable platform to demonstrate spin-dependent nonlinear effects.

Nonlinear spin-injection

We perform nonlinear spin-transport experiments on a van der Waals heterostructure of Graphene (Gr), encapsulated between a thick boron nitride (hBN) substrate and a trilayer hBN tunnel barrier with ferromagnetic cobalt contacts as shown in Figs. 1(a,b). We start by characterizing the tunnelling behaviour of the contacts. Contacts with(out) the tunnel-barrier show nonlinear(linear) current-voltage characteristics [inset of Fig. 1(c)] for an applied dc charge current $I$ and the measured voltage $V_c$ across the contact in a three-probe measurement geometry. Next, we probe the presence of nonlinear behaviour in the nonlocal signal $v_{\text{nl}}$ in a four-probe measurement geometry. For an input ac current $i$ at frequency $f=6$ Hz, $v_{\text{nl}}$ is measured using the scheme in Fig. 1(a), and its Fourier transform is shown in Fig. 1(c). For a linear device, an applied current at a certain frequency should yield a voltage at the same frequency alone. The appearance of voltage at integral multiples of the input-current frequency, the so called higher harmonics, is a smoking gun signature of nonlinearity. In our measurements, higher harmonics at $2f, 3f, ...$ appear in $v_{\text{nl}}$ only when the tunnel contact C1 is used as an injector (blue spectrum in Fig. 1(c)), and thus underline the crucial role of tunnel contacts for introducing nonlinearity in $v_{\text{nl}}$.

The concept of nonlinear spintronic measurements is schematically demonstrated in Fig. 1(d). For an input charge current $i + I$ at a ferromagnetic contact, higher harmonics in the spin-signal $v_s$ are measured at the output, due to the nonlinearity in the spin-injection process, present in a spintronic device. To probe the spin-dependent origin of nonlinearity in $v_{\text{nl}}$, we perform bias dependent nonlocal spin-valve (SV) measurements [1]. Here, we apply an ac+dc charge current $i + I$ and measure the 1st harmonic response of $v_{\text{nl}}$ via the lock-in detection method. An in-plane magnetic field $B_{||}$ is swept to switch

\[ v_s = p_{\text{inj}} R_s p_{\text{det}} i \]  

(1)

Here, $p_{\text{inj(det)}}$, the differential spin injection(detection) efficiency and $R_s$, the effective spin resistance of the spin transport channel [11] are constant, and thus the relation $v_s \propto i$ is established. Therefore, a nontrivial operation requiring nonlinearity can not be executed.
the magnetization-orientation of C1 and C2 from parallel to anti-parallel and vice-versa using the connection scheme in Fig. 1(a). Via SV measurements, we obtain background free pure spin-signal \( v_s = \frac{v_{nl}^{ap}}{2} \), where \( v_{nl}^{ap} \) is the nonlocal signal \( v_{nl} \) measured at the (anti-)parallel magnetization-direction alignment of the electrodes C1 and C2, as labeled in Fig. 2(a). In order to obtain the bias dependence of the spin-signal, we measure \( v_{nl}^{ap} \) as a function of \( I \), as shown in Fig. 2(d), and obtain \( v_s \). At \( I=0 \), there is a very small spin-signal \( v_s \sim 3 \text{ nV} \) (black dash line in Fig. 2 (d)). On applying \( I \) across the injector electrode, in line with the previous studies on Gr-hBN tunnel barrier systems [1, 15], \( v_s \) increases in magnitude and changes its sign on reversing the polarity of \( I \) (Fig. 2 (d)). Similarly, we also measure the 2\textsuperscript{nd} and 3\textsuperscript{rd} harmonic spin-signals via SV measurements and its bias dependence, as shown in Figs. 2(b,c,e,f). The unambiguous measurement of the higher harmonic spin-signals clearly suggests a presence of nonlinear processes in the spin-signal.

To confirm the spin-dependent origin of the nonlinearity in the spin-signal, we perform Hanle spin-precession measurements on 1\textsuperscript{st}, 2\textsuperscript{nd} and 3\textsuperscript{rd} harmonic spin-signals. Here, for a fixed in-plane magnetization configuration of the injector-detector electrodes (parallel or anti-parallel), as labeled in Figs. 2(a,b,c), a magnetic-field \( B_{\perp} \) is applied perpendicular to the plane of the device, as shown in Fig. 1(a). The injected in-plane spins diffuse towards the detector and precess around \( B_{\perp} \) with the Larmor frequency \( \omega_L \propto B_{\perp} \). The whole dynamics is given by the Bloch equation, \( D_s \nabla^2 \vec{\mu}_s - \frac{\vec{\mu}_s}{\tau_s} + \vec{\omega}_s \times \vec{\mu}_s = 0 \), with the spin diffusion constant \( D_s \), spin relaxation time \( \tau_s \), spin-accumulation \( \vec{\mu}_s = v_s/R_{\text{det}} \) in the transport channel, and the spin diffusion length \( \lambda_s = \sqrt{D_s \tau_s} \). The measured 1\textsuperscript{st}, 2\textsuperscript{nd} and 3\textsuperscript{rd} harmonic Hanle curves are fitted with the solution to the Bloch equation. From the fitting, we consistently obtain \( D_s \sim 0.02 \text{ m}^2\text{s}^{-1} \) and \( \tau_s \sim 650-700 \text{ ps} \) resulting in \( \lambda_s \sim 4 \mu \text{m} \) for the 1\textsuperscript{st} and higher harmonic
measurements in Figs 2(g-i). Since the spin transport parameters are the same for all harmonics, we conclude that the higher harmonic spin-signals do not have its origin in the spin-transport process, and pinpoint the origin of the spin-dependent nonlinearity to the spin-injection process.

To understand the concept of nonlinearity during spin-injection, we now develop an analytical framework. As the differential spin-injection polarization depends on the input dc bias current $I$, the expression for $p_{\text{nj}}$ using the Tailor expansion around $I = 0$ with a small ac charge current $i$ can be written as:

$$p_{\text{nj}}(i)|_{I=0} = p_0(1 + C_1i + C_2i^2 + ... )$$  \hspace{1cm} (2)

where $p_{\text{nj}} = p_0$ in the absence of nonlinear processes, which are enabled via the nonzero constants $C_1, C_2, ...$.
Now, using Eq. 1, we obtain:

$$v_s \propto p_0 i + p_0 C_1 i^2 + \ldots.$$  \hspace{1cm} (3)

which enables us to measure the presence of higher harmonic spin-signals $\propto i^2, i^3, \ldots$ due to the nonlinearity introduced by the spin-injection process in Eq. 2.

As shown in the spin-transport measurements in Fig. 2, the nonlinearity can be experimentally probed by using the mixed signal (ac+dc) measurements. When an input current $i + I$ is applied to such nonlinear system, the expression for the 1$^{\text{st}}$ harmonic spin-signal $v_s$, obtained by replacing $i$ with $i + I$ in Eq. 3, acquires a different function form (see Supplementary Material for derivation) and contains a bias $I$ dependent term:

$$v_s \sim \{p_0(1+2C_1 I)\} R_s p_{\text{det}} i.$$  \hspace{1cm} (4)

As a consequence of the nonlinearity present in the spin-signal (Eq. 3), additional terms with the mixing of $i$ and $I$ appear, and now $p_{\text{maj}} \sim p_0(1+2C_1 I)$ is obtained instead of $p_0$ (at $I=0$). For such case, one would expect a gain in $p_{\text{maj}} \propto I$. Indeed, corroborating with the hypothesis in Eq. 4, $v_s$ increases in magnitude with the applied dc bias $I$ and reverses its sign with the dc current polarity (Fig. 2(d)).

Similarly, the expressions for $n^{\text{th}}$ ($n \geq 2$) harmonic components of $v_s \propto (C_{n-1} + C_n I)^n$ due to nonzero $C_j$s are obtained using the mixed signal analysis (see Supplementary Material for detailed expressions). Here, the contribution from $C_{n-1}$, i.e. the $n^{\text{th}}$ order term in Eq. 3 would appear even if only the ac current is applied. In presence of a nonzero $I$, the higher order term $C_n$ would also contribute to the $n^{\text{th}}$ order spin-signal and introduce the dc bias dependence on the spin-signal.

For SV measurements in our device, we can only measure the even harmonic spin-signal, i.e. 2$^{\text{nd}}$ (Fig. 2(b,e)) and 4$^{\text{th}}$ (Supplementary Material) harmonic using the pure ac current injection ($I=0$). However, similar to the 1$^{\text{st}}$ harmonic spin-signal, higher odd (3$^{\text{rd}}$) harmonic spin-signal (Fig. 2(c,f)) can be measured unambiguously only with the application of the dc bias. When a nonzero $I$ is applied, the contribution of even harmonic signals couples to the odd harmonic spin-signals, and now the odd harmonic responses can also be measured. The dominance of only even harmonic components in the spin-signal is peculiar, and is not clear at the moment. Also, the bias-dependent behaviour of higher harmonic spin-signals can be explained via the expressions obtained from the mixed-signal analysis only near the zero-bias, where higher ($\geq 5^{\text{th}}$) harmonic components do not play a major role. A complete understanding of this behaviour warrants the inclusion of higher order terms in the expression for contact polarization as well as higher harmonic SV measurements for the estimation of the proportionality constant $C_j$($\geq 5^{\text{th}}$ harmonic).

**Analog signal-processing of spin-signal due to nonlinear effects**

The presence of nonlinearity which gives rise to signal-amplification, is fundamental to analog signal-processing operations [17]. In our spintronic device, we exploit the spin-dependent nonlinearity and demonstrate its applications straightforwardly by performing the spin analogues of well-established analog electronic operations.

**Amplitude modulation**

For amplitude modulation (AM) signal-processing [18], a modulating input $i_m$ along with a reference input $i_{\text{ref}}$, both having the same frequency $f$, are applied to a nonlinear element (Fig. 3(a)). As a result of signal mixing, for our nonlinear spintronic device, the output spin-signal $v_s \propto (i_{\text{ref}} + i_m)^2$ is detected at frequency $2f$. For a constant $i_{\text{ref}}$, if $i_m << i_{\text{ref}}$, the measured spin-signal will be $\propto i_m^2$, implying the effect will be linear in $i_m$ at the detection frequency $2f$ ($2^{\text{nd}}$ harmonic response), and we can realize an analog spin-signal multiplier.

In order to measure this effect, we inject $i_{\text{ref}} = 200$ nA and modulate $i_m$ in the range of 0-120 nA (both at $f=7$ Hz) at the injector (Fig. 1(a)). We measure the 2$^{\text{nd}}$ harmonic $v_s$ via SV measurements. The measured spin-signal is linear in $i_m$ (Fig. 3(b)) and thus the device acts as a spin-signal multiplier. For the other situation, i.e. when $i_m >> i_{\text{ref}}$, $v_s \propto (i_m)^2$. In this case, we fix $i_{\text{ref}}$=30 nA and modulate $i_m$ in the range 30-60 nA. The measured response of $v_s$ (Fig. 3(c)) clearly deviates from the earlier measured linear response in Fig. 3(c). However, due to the contribution of higher-order terms to the 2$^{\text{nd}}$ harmonic signal, the measurement in Fig. 3(c) is better explained by the 4$^{\text{th}}$ order polynomial fit instead of a parabolic fit.

**Heterodyne detection**

As another demonstration of signal-processing, in a heterodyne detection method the input signal frequencies are not equal, i.e. $f_m \neq f_{\text{ref}}$, and one obtains the signal at the heterodyne frequencies $f_{\text{ref}} \pm f_m$ at the output of the nonlinear element [18, 19]. In order to realize this operation, $i_{\text{ref}}$ at the frequency $f_{\text{ref}} = f$ and $i_m$ at $f_m = 2f$ are applied at the injector input (Fig. 3(d)). The nonlinear component of the spin-signal $v_s$ is $\propto (i_{\text{ref}} \sin(2\pi ft) + i_m \sin(2\pi 2ft))^2$. If $i_m=0$, one would expect the spin-signal $v_s$ at $2f$. Interestingly, for $i_m \neq 0, v_s \propto i_{\text{ref}} i_m$ can also be detected at the 1$^{\text{st}}$ ($f = 2f - f$) and 3$^{\text{rd}}$ ($3f = 2f + f$) harmonic components.

In our measurements, for $i_m=0$ and $i_{\text{ref}}=200$ nA ($f=7$ Hz), only the 2$^{\text{nd}}$ harmonic spin-signal is measured (}
Fig. 3(e)). When we also apply $i_{in}=150$ nA at the input frequency $2f$, spin-valve signals of similar magnitudes are detected at frequencies both at $f$ and $3f$ (Fig. 3(f)), which is a clear demonstration of heterodyne detection of spin-signals. Note that earlier there was no measurable odd (1st and 3rd) harmonic spin-signal at $I = 0$ (Figs. 2(d,f)) due to low injection-polarization/high-noise present in the signal. Now, using the heterodyne detection method we can clearly measure $v_s$ in the 1st harmonic even without applying $I$. In fact, this effect is equivalent to applying a dc current, as both heterodyne and ac+dc measurements couple the higher harmonic spin-signals to the 1st harmonic spin-signal. This method can be used to detect spin-signals at low frequencies where the spin-dependent noise would dominate in spintronic circuits [20, 21]. Furthermore, the method can also be used as an electrical analog of the heterodyne detection in the field on optical spin-noise spectroscopy [22, 23].

Nonlinear spin-to-charge conversion

So far we have demonstrated that the nonlinearity present in the spin-signal in a Gr/hBN heterostructure has its origin in the spin-injection process, not in the spin transport parameters. However, the nonlinearity in the spin-injection has an important consequence, and can amplify another nonlinear effect present in a small magnitude, i.e. spin-to-charge conversion [2, 3] in the spin-transport channel. The effect requires the energy dependent conductivity of the transport channel and the presence of spin-accumulation as prerequisites. A nonlocal charge-signal $v_c$ due to energy-dependent spin-to-charge conversion is given by:

$$v_c = C_0\mu_s^2 = C_0(p_{inj}R_s e)^2i^2,$$

where $C_0$ is a proportionality constant (see Supplementary Material for details), and we have used the relation $\mu_s = v_sc/p_{det}$ and Eq. 1 to obtain the $v_c-i$ dependence.

Now, to probe the spin-to-charge conversion effect and the spin-dependent origin of the nonlocal charge voltage, we perform Hanle measurements. Since the spin-to-charge conversion is a 2nd harmonic effect for the applied charge current $i$, we inject a pure ac current $i$ in the range 100-400 nA and measure the 2nd harmonic response of $v_{nl}^{ap}$ as a function of $B_\parallel$ using the measurement geometry in Fig. 1(a). In our measurements, we observe an asymmetry between the magnitudes of $v_{nl}^{ap}$ and $v_{nl}^{ap}$ in Figs. 4(a-c), which is present in a small magnitude for $i=100$ nA and grows rapidly for $i=400$ nA to such extent that the Hanle-dephasing of $v_{nl}$ is measured properly only in the parallel configuration.
To understand the origin of this asymmetry, we plot the nonlocal charge voltage $v_c = (v_{n}^{ap} + v_{n}^{ap})/2$ (Fig. 4(e)) and the spin-signal $v_s = (v_{n}^{ap} - v_{n}^{ap})/2$ (Fig. 4(d)). The Hanle like shape of $v_c (B_{\perp})$ in Fig. 4(e) immediately confirms that indeed the nonlocally measured charge voltage $v_c$ has the spin-dependent origin, and is reduced to zero in the absence of spin-accumulation (at $B_{\perp} \sim 40$ mT). Next, due to its square dependence on $\mu_s$ in Eq. 5, $v_c$ should decay with the characteristic spin-relaxation length $\lambda_s/2$ instead of $\lambda_s$ [2]. In order to verify this hypothesis (Eq. 5), we fit $v_c - B_{\perp}$ dependence in Fig. 4(e) with the solution to the Bloch equation, and obtain $\lambda_s \sim 2 \mu m$, which is about half the spin relaxation length obtained via the Hanle spin-precession measurements on the spin-signal $v_s$ (Fig. 4(d)). The same effect appears in the 1st harmonic $v_c$ due to its coupling with the 2nd
harmonic effect in presence of a nonzero $I$ (see Supplementary Material). In this way, we unambiguously establish the spin-dependent origin and the square dependence of the nonlocal charge voltage on spin-accumulation via Hanle measurements.

Lastly, the $v_c-i$ dependence is plotted in Fig. 4(f). The dark (light) grey dashed line is the calculated magnitude of $v_c$ while considering the contribution from nonlinear (linear) spin injection with $I^4(I^2)$ dependence on the injected current (see Supplementary Material for details). The measured data is in close agreement with the calculated $v_c$ due to the nonlinear spin-injection, and is better fitted with a 4th order polynomial than a parabolic function. Clearly, such efficient spin-to-charge conversion cannot be explained only via the linear spin-injection process, and the contribution from the nonlinear processes has to be taken into account. In conclusion, Gr/hBN heterostructures due to the presence of nonlinear spin-injection offer a highly efficient platform to probe nonlinear spin-to-charge conversion effect. The interaction of the two nonlinear effects produces a measurable effect without needing any additional effect such as spin-orbit coupling [26, 27].

To summarize, we, for the first time demonstrate the presence of spin-dependent nonlinearity in a spintronic device via all electrical measurements. This effect is the key ingredient in signal-processing, and opens up the portal for the development of the field of analog spintronics, following the pathway of the electronic revolution. Our results suggest that nonlinearity can be exploited in multiple ways to manipulate spin-information such as via complex signal-processing and spin-to-charge conversion, and develop advanced multi-functional spintronic devices [2–5, 28] and spin-based neuromorphic computing [29].

**METHODS**

**a. Sample fabrication**

We prepare a fully hBN encapsulated graphene stack via a dry pick-up transfer method. The hBN (thickness~7 nm) and graphene flakes are exfoliated on SiO$2$/Si substrate and identified via optical contrast analysis using an optical microscope. The thickness of hBN layer is measured via the atomic force microscopy and is ~9 nm for the bottom hBN substrate and 0.9-1.0 nm (3L) for the top hBN layer. For the stack preparation, the 3L-hBN flake is brought in contact with a visco-elastic PDMS (polydimethylsiloxane) stamp which has a sticky PC (polycarbonate) film attached to it. During the contact, the whole assembly is heated and the hBN is picked up by the PC film. Following the same step, the Gr flake is picked up by the hBN flake on the PC film due to the van der Waals interaction between these two layers. In the last step, the thick hBN flake on the SiO$_2$ substrate is brought in contact with the Gr/3L-hBN on the PC film, the whole assembly is heated up to 150°C and the PC film with the Gr/3L-hBN is released on to the bottom hBN substrate. Afterward, the bottom-hBN/Gr/3L-hBN stack is put in chloroform solution at room temperature to dissolve the PC film. In order to remove the remaining polymer residues on top of the top 3L-hBN layer, the stack is annealed at 250°C in Ar-H$_2$ environment for 7 hours.

**b. Device Fabrication**

The electrodes are patterned via the electron-beam lithography on the PMMA (poly-methyl methacrylate) spincoated sample. Then the sample is developed in a MIBK:IPA solution for 60 seconds in order to remove the polymer from the electron-beam exposed area. Next, to obtain the spin-sensitive electrodes, 65 nm thick cobalt is deposited on the sample via electron-beam evaporation. In order to prevent the oxidation of cobalt, a 3 nm thick layer of aluminium is deposited on top. The residual metal on top of the polymer is removed by performing the lift-off in hot acetone at 40°C.

**c. Measurements**

Measurements were performed both at 4K (Helium temperature) and room temperature in vacuum in a flow cryostat. Differential ac signal measurements were performed using low frequency lock-in detection method. For mixed signal (ac+dc) measurements and back-gate application, Keithley 2410 dc source was used.

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[1] Shockley, W., Sparks, M. & Teal, G. K. p-n Junction Transistors. *Phys. Rev.* **83**, 151–162 (1951).

[2] Datta, S. & Das, B. Electronic analog of the electrooptic modulator. *Appl. Phys. Lett.* **56**, 665–667 (1990).

[3] Gmitra, M. & Fabian, J. Proximity Effects in Bilayer Graphene on Monolayer WSe$_2$: Field-Effect Spin Valley Locking, Spin-Orbit Valve, and Spin Transistor. *Phys. Rev. Lett.* **119**, 146401 (2017).

[4] Zeng, M. *et al.* Graphene-based bipolar spin diode and spin transistor: Rectification and amplification of spin-polarized current. *Phys. Rev. B* **83**, 115427 (2011).

[5] Acremen, Y. *et al.* An amplifier concept for spintronics. *Appl. Phys. Lett.* **93**, 102513 (2008).

[6] Wang, Y., Liu, Y. & Wang, B. Graphene spin diode: Strain-modulated spin rectification. *Appl. Phys. Lett.* **105**, 052409 (2014).

[7] Flatt, M. E. *et al.* Theory of semiconductor magnetic bipolar transistors. *Appl. Phys. Lett.* **82**, 4740–4742 (2003).
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AUTHOR CONTRIBUTIONS

S.O., M.G. and B.J.v.W. conceived the experiment. S.O., K.W. and T.T. carried out the sample fabrication. S.O. and M.H.D.G. carried out the experiment. S.O., M.G.,M.H.D.G. and B.J.v.W. carried out the analysis and wrote the manuscript. All authors discussed the results and the manuscript.
Supplementary Information

I. MODEL FOR NONLINEAR SPIN-INJECTION

Current/voltage bias dependence of the spin-injection efficiency across the cobalt/hBN/Gr contact introduces nonlinearity in the spin-injection process. As discussed in the main text, the differential polarization depends on the input bias current $I$, the expression for $p_{\text{inj}}$ using the Tailor expansion around $I = 0$ can be written as:

$$p_{\text{inj}}(i) = p_0(1 + C_1 i + C_2 i^2 + ...)$$  \hfill (S1)

where $p_0$ is the unbiased differential contact polarization. The spin-signal in the nonlocal geometry is:

$$v_s = \{p_{\text{inj}}\} \times R_s \times p_{\text{det}} i.$$  \hfill (S2)

Here, $p_{\text{det}}$ is the unbiased detector polarization, $R_s$ is the effective graphene spin resistance. By substituting Eq. S1 into Eq. S2, we obtain the following expression for $v_s$:

$$v_s = \{p_0(1 + C_1 i + C_2 i^2 + ...)i\} \times R_s \times p_{\text{det}}$$

$$\quad = \{p_0 R_s \times p_{\text{det}}\} i + \{p_0 C_1 R_s \times p_{\text{det}}\} i^2$$

$$\quad + \{p_0 C_2 R_s \times p_{\text{det}}\} i^3 + ...$$  \hfill (S3)

Due to the presence of nonlinearity in the spin-injection process, even the 2nd, 3rd and 4th harmonic spin-signals can be measured.

II. MIXED-SIGNAL ANALYSIS

The nonlinearity in the spin-signal can be measured via mixed-signal analysis which is a well established framework in the field of analog electronic-circuit design. We use this tool to measure and analyze the nonlinearity present in the spin-injection process.

When two independent inputs are supplied to a linear system, its response will be a linear combination of the input signals. However, this is not the case when the system possesses nonlinearity, and additional contributions would appear due to the mixing of the independent input signals. In order to measure the response of the ac and dc input signals and their mixing, we apply a charge current $I + i \sin \omega t$. We apply a dc current using a home built dc current source and the ac current using a lock-in source across the injector electrodes. Since we know from the measurements presented in the main text that $R_s$ and $p_{\text{det}}$ remain constant, for sake of simplicity we omit the constants in Eq. S3, and to explain the analysis, we assume $p_{\text{inj}} = p_0(1 + C_1 I)$ and omit the higher order terms. Now, $v_s$ is:

$$v_s \propto \{p_0(1 + C_1(I + i \sin \omega t))\} \times (I + i \sin \omega t)$$

$$\quad \propto \{p_0(I + i \sin \omega t)\} + p_0 C_1 \times ((I + i \sin \omega t)^2)$$

$$\quad \propto \{p_0(I + C_1 I^2)\} + \{p_0(1 + 2C_1 I) i \sin \omega t\}$$

$$\quad + \{p_0 C_1 i^2 \sin^2 \omega t\}$$  \hfill (S4)

$v_s$ in Eq. S4 has three distinct contributions, a dc, a 1st harmonic (i.e. $\propto \sin \omega t$) and a 2nd harmonic ($\propto \sin^2 \omega t$) contribution, separated in curly brackets. In a lock-in measurement, if an ac current $i$ is applied to the sample at a lock-in reference frequency $f = \frac{\omega}{2\pi}$, only the components of $v_s$ appearing at frequency $f$ or at higher harmonics $2f, 3f, ...$ would be measured via the lock-in detection method. Other contributions are filtered out and are not measured via the lock-in amplifier. In order to do so, the sample output $v_s$ in Eq. S4 at the lock-in input is multiplied with the reference signal $\propto \sin n \omega t$, where $n = 1, 2, ...$ in order to measure the 1st, 2nd, ... harmonic contributions. Then the output is low-pass filtered to obtain a dc output.

In order to filter out the 1st harmonic contribution, $v_s$ in Eq. S4 is multiplied with the reference signal $\sin \omega t$, and $v_s \propto \sin \omega t$ is only filtered out and measured in the 1st harmonic response:

$$v_s = \{p_0(1 + 2C_1 I)\} \times R_s \times p_{\text{det}} i$$  \hfill (S5)

Here, we would like to emphasize that due to the nonlinear term present in contact polarization, i.e. because of a nonzero $C_1$, contact polarization is not equal to $p_{\text{inj}} = p_0$ anymore and is modified to $p_{\text{inj}} = p_0(1 + 2C_1 I)$. Therefore, in presence of the nonlinearity the dc and differential contact polarization will not be equal and the differential one may exceed the dc polarization [1].

Now, in the same way, the 2nd harmonic component of $v_s$ can be filtered out by multiplying $v_s$ in Eq. S4 with $\sin 2\omega t$:

$$v_s = \{p_0 C_1\} \times R_s \times p_{\text{det}} i^2$$  \hfill (S6)

It is evident from the expression in Eq. S6 that if $C_1 \neq 0$, the spin-valve effect would be observed in the 2nd harmonic measurements as well.

Using the analysis presented above, higher order nonlinearity can be included in the contact polarization $p_{\text{inj}}$ with nonzero $C_2, ...$ as in Eq. S1 in the same way. Without the loss of generality, following the arguments presented above, one would expect the spin-valve effect to appear in the 3rd harmonic measurements for $C_2 \neq 0$ and the $C_2 I$ dependent terms in the 1st and 2nd harmonic spin-signals, as can be seen in Fig.2 of the main text. In this way, for highly nonlinear spin-injection processes, there will be contributions of higher order spin-injection processes appearing in the low-order terms due to the coupling of higher order processes with the charge current.
III. NONLINEAR SPIN-TO-CHARGE CONVERSION

Ferromagnets (FM) have a nonzero spin-dependent conductivity \( \sigma_s \), i.e. spin-up and spin-down electrons in FM materials have different conductivity \( \sigma^\uparrow \) and \( \sigma^\downarrow \) where \( \sigma_s = \sigma^\uparrow - \sigma^\downarrow \). In presence of a nonzero spin-current, i.e gradient of the spin-accumulation \( \mu_s = (\mu^\uparrow - \mu^\downarrow)/2 \), it gives rise to a charge voltage \( v_c \propto \sigma_s \nabla \mu_s \) in the FM. However, nonmagnets (NM) have \( \sigma_s = 0 \).

Because of energy-dependent density of states in graphene, in presence of a large spin-accumulation \( \mu_s \), spin-up and spin-down electrons experience different conductivity [2, 3]. Therefore, in spite of being a nonmagnet, graphene develops a nonzero spin-polarization \( P \) pseudo away from the Fermi level, and behaves as a pseudoferromagnet. As a consequence, a nonlocal charge voltage \( v_c \) is developed along the spin-transport channel length:

\[
v_c = -P_d (\mu_s/e)
\]

where \( P_d \) is the spin-to-charge conversion efficiency and can be represented as:

\[
P_d = -\mu_s \times \frac{1}{\sigma} \times \frac{\delta\sigma}{\delta E}
\]

where \( \sigma \) is the energy-dependent conductivity of graphene. Now, \( v_c \) can be written as:

\[
v_c = \frac{1}{\sigma} \times \frac{\delta\sigma}{\delta E} \times \frac{(\mu_s)^2}{e}
\]

\[
= C_0 \mu_s^2 \propto i^2
\]

The proportionality constant \( C_0 \) can be derived from the carrier-density dependent conductivity measurements of graphene and the density of states in graphene (bilayer graphene in our case). The procedure is as follows:

The total number of carriers \( n \) can be calculated using the relation:

\[
n = \int_0^{E_F} \nu(E)dE
\]

where the density of states \( \nu(E) \) of the BLG is:

\[
\nu(E) = \frac{g_s g_v}{4\pi^2 \hbar^2 v_F^2} (2E + \gamma_1)
\]

Here \( g_s \) and \( g_v \) are electron spin and valley degeneracy (=2), \( \hbar \) is the reduced Planck coefficient, \( v_F = 10^6 \text{ m/s} \) is the electron Fermi velocity, and \( \gamma_1 = 0.37 \text{ eV} \) is the interlayer coupling coefficient. We extract the carrier density in graphene from the Dirac measurements, and use it calculate \( \frac{\delta\sigma}{\delta E} \) as a function of \( n \) using Eq. S10 and Eq. S11.

Then, we can easily estimate \( C_0 \) using Eq. S9 for our sample. Using this procedure, we obtain \( C_0 \) as a function of the back-gate voltage \( V_{bg} \) (Fig. S1). Since, we perform all measurements at \( V_{bg} = 0 \text{ V} \), we use \( C_0 = 15 \text{ V}^{-1} \) for further calculations.

![FIG. S1. \( R_{sq} \) (left y-axis)-\( V_{bg} \) dependence of graphene (red). On the right y-axis the spin-to-charge conversion efficiency \( C_0 - V_{bg} \) dependence (in black) is plotted. \( C_0 \) at \( V_{bg}=0 \text{ V} \) is marked with a solid black dot.](image-url)

III. MODEL FOR SPIN TO CHARGE CONVERSION

We know, from Eq. S9, the spin-accumulation induced charge voltage \( v_c = C_0 \mu_s^2 \). If an ac charge current \( i \) is applied across the injector electrode, it creates a spin accumulation \( \mu_s = p_{i\text{nj}} R_s \) underneath the injector electrode, which is measured at a distance \( L \) away from the injector electrode.

\[
v_c = C_0 \mu_s^2 = C_0 (p_{i\text{nj}} R_s e)^2
\]

where \( C = C_0 (R_s e)^2 \). While deriving the expression for \( v_c \), we also consider the role of the nonlinear spin-injection and assume \( p_{i\text{nj}} = p_0 (1 + C_1 i) \), and substitute this expression into Eq. S15:

\[
v_c = C p_0^2 (1 + C_1 i)^2 \frac{\delta\sigma}{\delta E}
\]

\[
= C p_0^2 (i^2 + 2C_1 i^3 + C_1^2 i^4)
\]

Now, we can perform the mixed signal analysis on the expression in Eq. S14 by replacing \( i \) with \( I + i \sin \omega t \) in the same way as described in supplementary section II and obtain expressions for the 2nd harmonic components of \( v_c \):
\[ v_c^{2\text{nd}} = C p_i^2 \left( i^2 + 6C_1 I i^2 + 6C_2^2 I^2 i^2 + C_4^2 i^2 \right) \cos 2\omega t \]

Here, we would like to remark that for \( I = 0 \), we would expect \( v_c^{2\text{nd}} \propto i^2 \) for small \( i \) and \( v_c^{2\text{nd}} \propto i^4 \) for the large \( i \) values. The consequences of this dependence are significant as because of a nonzero \( C_1 \), at large \( i \) values, \( v_c \propto i^4 \) while \( v_c \propto i^2 \) (Fig. 4 in the main text). Therefore, at large \( i \) the spin-accumulation induced charge-voltage \( v_c \) would be comparable to, and can even surpass the spin-signal \( v_s \).

**SPIN TO CHARGE CONVERSION IN 1st HARMONIC RESPONSE**

As explained in Sec.III, spin-to-charge conversion is a nonlinear effect, and is measured as higher harmonic of the nonlocal charge signal. However, similar to the nonlinear spin transport measurements, when a dc charge current \( I \) is injected along with \( i \), due to the mixing between \( i \) and \( I \), we can also measure \( v_c \) in the 1st harmonic response. The expression for 1st harmonic component of \( v_c \), obtained by using the mixed signal analysis is:

\[
v_c^{\text{1st}} = C p_i^2 \left( 2I i + 6C_1 I^2 i + \left(3/2\right) C_1 i^3 \right) + 3C_2^2 I^3 i + 4C_4^2 I^5 i \sin \omega t \\
\simeq C p_i^2 I \left( 1 + 3C_1 I + 2(C_1 I)^2 \right) \quad (i << I).
\]

Here, the terms with \( C_1 \) in the expression in Eq. S15 appear due to the nonlinear spin-injection process. If \( C_1 I > 1 \), the term \( \propto (C_1 I)^2 \) will dominate and set amplification factor for the spin-to-charge conversion effect in the 1st harmonic response, which is absent for linear spin-injection. Now, \( v_c \propto C p_i^2 I (C_1 I)^2 \), and due to the nonlinearity present in the spin-injection process, we would expect an amplification in the spin-to-charge conversion effect in the 1st harmonic signal, proportional to \( (C_1 I)^2 \).

In order to verify this hypothesis, we revisit the 1st harmonic Hanle measurements, and obtain \( v_c \) as an average of \( v_{\text{nl}}^0 \) and \( v_{\text{nl}}^{\text{ap}} \). We first present the case when no bias is applied at the injector. For \( I=0 \), we expect \( v_c = 0 \) and symmetric parallel and anti-parallel Hanle curves. Since we cannot measure any spin-signal clearly while using the tunnel contact C1 as an injector without biasing it, due to the presence of large noise and a small spin-signal due to small contact-polarization, we use the transparent contact C2 as a injector and C1 as a detector (Fig. 1(a)). Now, C1 can be biased with \( I \) to enhance its spin-detection efficiency \( p_{\text{det}} \) and the spin-signal can be measured. Since \( I=0 \) at the injector, there should be no coupling between the 1st and 2nd harmonic \( v_c \) and the parallel and anti-parallel Hanle signals should be symmetric. In our measurement while using C2 as an injector and C1 as a detector we measure roughly symmetric Hanle curves with respect to the background (black dashed line) for the parallel and anti-parallel configurations (Fig. 4(d)). However, there is no asymmetry expected for this case. The reason for such behavior is not clear to us at the moment.

Now, when we use the tunnel contact C1 as an injector and C2 as a detector, and inject a charge current \( I + i \), as expected we see a huge asymmetry between the magnitudes of parallel and the anti-parallel Hanle signals in Fig. S2(b,c) for \( I = \pm 250 \text{ nA} \) due to the presence of spin-to-charge conversion effect. Simlar to the 2nd harmonic measurements in Fig. 4(c) in the main text, the spin-accumulation induced charge signal which is the average of the parallel and anti-parallel spin-signals is comparable to the spin-signal. Due to the dominant 2nd order spin-injection and its contribution to the 1st harmonic spin-to-charge conversion, the higher order terms in Eq. S15 contribute significantly, and we also see the sign-reversal of \( v_c \) with the polarity of \( I \). In order to appreciate the role of the nonlinear spin-injection to measure such effect, we also present a similar case for spin-injection in a different sample using a 2L-hBN, in ref. [1] where, where the nonlinear constant \( C_1 \sim 10^5 \text{A}^{-1} \) is not dominant enough compared to \( C_1 \sim 10^8 \text{A}^{-1} \) for 3L-hBN. Here, even for high enough \( I = \pm 25 \mu \text{A} \), \( v_c \) is significantly small compared to the spin-signal \( v_s \) (Fig. S3), where \( v_c \) and \( v_s \) are of similar order magnitude. Therefore, we also do not measure a strong modulation in Hanle shapes in Fig. S3 as in Fig. S2 for nonzero \( I \). However, the asymmetry between the magnitudes of parallel and anti-parallel Hanle curves, along with the sign reversal in \( v_c \) with the polarity of \( I \) is consistently present in both measurements.

We would also like to remark that the observed behavior is not due to the contribution of outer injector/detector FM electrodes to the measured spin-signal. For nonlocal SV measurements, we consistently observe only two distinct levels in the spin-valve effect corresponding to parallel and anti-parallel configuration of the injector-detector pair. It confirms the contribution of only one FM injector and one detector in contrast with the recently reported two-probe spin-transport measurements in ref. [1, 4] where both FM electrodes act as spin-injector and detector contacts and result in asymmetric Hanle curves for parallel and anti-parallel configurations.

Lastly, similar to the 2nd harmonic spin-to-charge conversion effect, shown in Fig. 4(c) of the main text, we also plot the 1st harmonic \( v_c-B_\perp \) dependence, and obtain the same information. The Hanle-like magnetic-field dependence of \( v_c \) in Fig. S2(e) confirms its spin-accumulation induced origin. The fitting of the Hanle curves in Fig. S2(d) and Fig. S2(e) results in \( \lambda \sim 4 \)
FIG. S2. 1\textsuperscript{st} harmonic measurements (a) $R_{nl}^{p(ap)} = \frac{v_{p(ap)}}{i}$ are roughly symmetric with respect to the background (black dashed line) for $i=20\ \mu A$ and $I=0$ at the injector. Here, the transparent contact C2 is used as an injector and the tunnel contact C1 is used as a detector. When the tunnel contact is used as an injector, a strong asymmetry is measured between $R_{nl}^{p}$ (green) and $R_{nl}^{ap}$ (pink) with respect to the background for (b) $I=+250\ nA$ and (c) $I=-250\ nA$ due to the coupling of the 2\textsuperscript{nd} harmonic spin-to-charge conversion effect to the applied dc bias $I$. 1\textsuperscript{st} harmonic (d) spin-signal $v_c$, (e) Nonlocal charge-signal $v_c-B_\perp$ dependence. The data is symmetrized and a constant background is subtracted from the raw data. (f) Summary of $v_c-v_s$ dependence. The measurements are performed at 4K.

µm and $\sim 2\ \mu m$, respectively. By fitting the $v_c-B_\perp$ dependence in Fig. S2(e), according to the expectation $v_c \propto v_s^2$, $\lambda_s \sim 2\ \mu m$ is obtained which is half of the spin-relaxation length obtained from the spin-signal $v_s$, and again corroborates the square dependence of the nonlocal charge-signal on spin-accumulation, as obtained in the 2\textsuperscript{nd} harmonic measurements in the main text.

4\textsuperscript{th} HARMONIC SPIN SIGNAL

We also measure the 4\textsuperscript{th} harmonic component of the spin-signal for the input ac current $i=100\ nA$. The spin-valve effect is shown in Fig. S4(b). Similar to the 2\textsuperscript{nd} harmonic spin-signal, the 4\textsuperscript{th} harmonic spin-signal can be measured unambiguously without applying any dc current. As soon as a finite dc bias $I$ is applied along with the ac charge current $i$, again in line with the bias-dependence of the 2\textsuperscript{nd} harmonic spin-signal (Fig. 2(e) in the main text), the magnitude of the 4\textsuperscript{th} harmonic signal is also reduced as shown in Fig. S4(a).

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[1] Gurram, M., Omar, S. & Wees, B. J. v. Bias induced up to 100% spin-injection and detection polarizations in ferromagnet/bilayer-hBN/graphene/hBN heterostructures. Nature Communications \textbf{8}, 248 (2017).

[2] Vera-Marun, I. J., Ranjan, V. & van Wees, B. J. Nonlinear interaction of spin and charge currents in graphene. Phys. Rev. B \textbf{84}, 241408 (2011).
FIG. S3. 1st harmonic measurements for parallel (green) and anti-parallel (pink) configurations, using a bilayer hBN tunnel barrier as a spin-injector at $i=3 \mu A$ and $I=(a)$ 25 $\mu A$ (b) 5 $\mu A$ and (c) -25 $\mu A$, and the corresponding $v_c$ at (d), (e) and (f) respectively. The data is symmetrized and a constant background is subtracted from the raw data. The measurements are performed at RT.

[3] Vera-Marun, I. J., Ranjan, V. & van Wees, B. J. Nonlinear detection of spin currents in graphene with non-magnetic electrodes. Nature Physics 8, 313–316 (2012).

[4] Gurram, M., Omar, S. & Wees, B. J. v. Electrical spin injection, transport, and detection in graphene-hexagonal boron nitride van der Waals heterostructures: progress and perspectives. 2D Mater. 5, 032004 (2018).
FIG. S4. (a) 4th harmonic spin signal (orange) and its bias dependence. The (anti) parallel, data in (blue)red is plotted against the right-y axis. (b) 4th harmonic spin-valve signal