Imaging charge migration in chiral molecules using time-resolved x-ray diffraction

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Four-dimensional imaging of charge migration is crucial to the understanding of several ubiquitous processes in nature. The present work focuses on imaging of charge migration in an oriented epoxypropane: a chiral molecule. A linearly polarized pulse is used to induce the charge migration, which is imaged by time-resolved x-ray diffraction. It is found that the total time-resolved diffraction signals are significantly different for both enantiomers. Furthermore, a connection between time-resolved x-ray diffraction and the electronic continuity equation is discussed by analyzing the time-dependent diffraction signal and the time derivative of the total electron density in the momentum space.

I. INTRODUCTION

X-ray diffraction is the method of choice when it comes to extracting the real-space structure of solids and molecules with atomic-scale spatial resolution. Thanks to technological advances that have made it possible to generate intense ultrashort pulses from novel x-ray source: x-ray free-electron lasers (XFELs). X-ray pulses with pulse duration of a few femtoseconds are routinely employed to perform various kinds of experiments at different XFEL sources. Moreover, generation of attosecond x-ray pulses was demonstrated experimentally in recent years. These ultrashort x-ray pulses have enabled extension of static x-ray diffraction into the time domain with exceptional temporal resolution. Time-resolved x-ray diffraction (TRXD) within a pump-probe configuration is an emerging method to obtain snapshots of a temporarily evolving electronic charge distribution in matter with spatiotemporal resolution. An electronic movie of ultrafast charge migration can be made by putting the recorded snapshots together as a function of pump-probe delay time.

In this work, we investigate imaging of pump-induced charge migration in a chiral molecule using TRXD. Oriented epoxypropane (1,2-propylene oxide) is used as a prototypical system. The notion of chirality is omnipresent in nature. Understanding the chirality is essential for a broad range of sciences including origin of homochirality on earth. A molecule without inversion symmetry or a symmetry plane which is not superimposable with its own mirror image is known as a chiral molecule. A pair of such chiral molecules is known as enantiomers. Enantiomers exhibit identical physical properties, but show a strong enantiomeric preference during chemical and biological reactions. Discerning the enantiomeric excess and handedness of chiral molecules is crucial in chemistry, biology and pharmaceuticals.

Confirming the handedness of chiral molecules by determining their spatial arrangement is known as absolute configuration determination. X-ray crystallography is one of the most reliable methods to determine the absolute configuration. In recent years, other methods such as microwave spectroscopy, Coulomb-explosion imaging, high-harmonic generation, vibrational circular dichroism, and photoelectron circular dichroism have been employed to discern enantiomers. Here we demonstrate that TRXD within the pump-probe configuration offers an alternative method to probe the handedness of chiral molecules.

In previous work, we demonstrated that the diffusion signal, obtained from TRXD, is related to the time derivative of the momentum-space density. When a pump pulse induces a charge migration in matter, the time-dependent charge dynamics is associated with the electronic flux densities by obeying the quantum continuity equation. Time-resolved x-ray diffraction thereby encodes indirectly the information about electronic flux densities accompanying charge migration. The flux densities contains crucial mechanistic information about non-equilibrium electron dynamics in matter. In recent years, several proposals have been put forward to image the flux densities and ring currents associated with charge migration using TRXD, ultrafast x-ray absorption and high-harmonic generation. The present work shows that TRXD and electronic flux density analysis provide complementary information on the charge migration in oriented chiral molecules driven by linearly polarized light. The intrinsic dynamics and its detection are drastically different, and the complementary information can thus be used to discriminate the enantiomers.
II. MODELS AND METHODS

We simulate ultrafast electron dynamics using the hybrid time-dependent density functional theory-configuration interaction (TDDFT-CI) methodology [48]. This combination of methods provides a good balance between accuracy and computational efficiency. A generic N-electron wave packet $\Psi(r_N, t)$ is represented at any given time $t$ as a linear combination of the ground state Slater determinant and singly excited many-body excited states. In spin-free representation, the wave packet takes the form

$$\Psi(r_N, t) = \sum_{k=0}^{N_{\text{states}}} C_k(t) \Phi_k(r_N).$$

In the case of field-free temporal evolution, $C_k(t) = c_k \exp(-iE_k t)$. This wave packet evolves according to the many-electron time-dependent Schrödinger equation

$$i \partial_t \Psi(r_N, t) = \left[ \hat{H}_0 - \mu \cdot F(t) \right] \Psi(r_N, t).$$

Here, $\hat{H}_0$ is the field-free Hamiltonian within the Born-Oppenheimer approximation. The field-molecule interaction is treated in the semi-classical dipole approximation, with $\mu$ the molecular dipole operator and $F(t)$ an applied external electric field.

The lowest-lying excited eigenstates $\Phi_k(r_N)$ of the many-body electronic Hamiltonian are calculated as linear combinations of Slater determinants. Each excited $N$-electron state is expressed as a linear combination of singly excited configuration state functions

$$\Phi_k(r_N) = \sum_{a,r} D_{a,r,k}^r \Phi^r_a(r_N).$$

The configuration state functions $\Phi^r_a(r_N)$ are spin symmetrized combinations of excited Slater determinants. They are defined with respect to the Kohn-Sham ground state $\Phi_0(r_N)$, by taking an electron from an occupied molecular orbital $a$ to a virtual molecular orbital $r$.

In the hybrid TDDFT-CI method, all expansion coefficients $\{D_{0,k}, D_{a,k}\}$ are obtained from linear-response TDDFT. This step is performed using standard quantum chemistry programs. The information from the quantum chemistry package is postprocessed with the open-source toolbox detCI@ORBKIT. The contributions of the different Slater determinants extracted from the quantum chemistry programs are first pruned by removing all contributions below some numerical threshold (here chosen as $10^{-5}$) and then renormalized. In the basis of pseudo-CI eigenfunctions chosen for the propagation, the Hamiltonian is considered diagonal. The matrix elements of the dipole moment operator in Eq. (2) are computed by numerical integration. Finally, the time-evolution of the coefficients $C_k(t)$ in Eq. (1) is performed by direct numerical integration of Eq. (2) using a preconditioned adaptive step size Runge-Kutta algorithm [50].

In this work, all $N_{\text{states}} = 31$ lowest-lying excited states below the ionization threshold are used to obtain convergence, checked by repeating the laser-driven dynamics simulations with $N_{\text{states}} = \{16, 21, 26, 31\}$. The states are computed using the CAM-B3LYP functional [51] and aug-cc-pVTZ basis sets [52] on all atoms, as implemented in Gaussian16 [53]. The motion of nuclei are typically much slower in comparison to the electronic motion and therefore nuclei are treated as frozen in this work.

Integrating the time-dependent many-electron wave packet in Eq. (1) leads to the one-electron quantum continuity equation

$$\partial_t \rho(r, t) = -\nabla \cdot j(r, t).$$

Here, $\rho(r, t)$ is the one-electron density and $j(r, t)$ the electronic flux density [54]. From the many-body wavefunction, the expectation value of the one-electron density operator

$$\hat{j}(r) = \sum_k \delta(r - r_k)$$

yields the one-electron density. The Dirac delta distribution $\delta(r - r_k)$ evaluates the probability of finding electron $k$ with position $r_k$ at a point of observation, $r$. The expectation value of the operator

$$\hat{j}(r) = \frac{1}{2} \sum_k \left( \delta_k(r) \hat{p}_k + \hat{p}_k^\dagger \delta_k(r) \right)$$

yields the flux density, where the momentum operator $\hat{p}_k = -i\nabla_k$ of electron $k$ is applied either to the right or to the left. The molecular orbitals to compute the integrals are expressed as linear combinations of atom-centered Gaussian functions, and all integrals are computed analytically. The charge density and flux density thus obtained satisfy very accurately the continuity equation as given in Eq. (3). Details on the computation of the one-electron integrals from the many-body wavefunction using the detCI@ORBKIT toolbox [55–57] are given elsewhere.

When the probe pulse duration is much shorter than the timescale of the charge migration, the TRXD signal can be simulated using the expression for the differential scattering probability (DSP) [58]

$$\frac{dP}{d\Omega} = \frac{dP_r}{d\Omega} \sum_j \left| \int dr \langle \Phi_j | \hat{n}(r) | \Psi(T) \rangle e^{-iQ \cdot r} \right|^2,$$

where $\frac{dP_r}{d\Omega}$ is the Thomson scattering cross section of a free electron. The signal probes the coherences between eigenstates of the unperturbed Hamiltonian, $|\Phi_k\rangle$, contained in an electronic wave packet $|\Psi(T)\rangle$ with $T$ the pump-probe delay time. In addition, $Q$ is the photon momentum transfer and $\hat{n}(r)$ is the electron density operator. The summation over $j$ includes all zeroth-order
states included in the dynamics, which amounts to detecting all the scattered photons within a given solid angle, irrespective of the mean photon energy.

After the pump pulse and in the absence of an external field, the time-dependent coefficients in Eq. (1) simplify to the analytical form containing an amplitude and energy-dependent phase. At $T = 0$, Eq. (7) reduces to the time-independent diffraction signal as

$$\frac{dP}{d\Omega} = \frac{dP_e}{d\Omega} \sum_j \sum_k c_k \int dr \langle\Phi_j|\hat{n}(\mathbf{r})|\Phi_k\rangle e^{-iQ \cdot \mathbf{r}}. \quad (8)$$

As evident from this equation, the time-independent diffraction signal is emerging from the joint contribution of the elastic and time-independent inelastic parts of the total diffraction signal. This term serves as a constant background in TRXD. To image the charge migration, we will present time-dependent difference diffraction signals where the total diffraction signal at zero delay time is subtracted from the subsequent delay times.

References [59, 60] discuss the different roles of time-independent and time-dependent diffraction signals from the total diffraction signal. Moreover, detailed discussions about probing electronic coherences in the wavepacket have been documented in Refs. [9, 61]. Furthermore, the time resolution in TRXD depends on several factors such as temporal duration on x-ray pulse, jitter between pump and probe pulses, and pump-probe time delay.

All many-electron dynamical simulations are performed using in-house codes [50, 62-65]. The integrals required to compute the TRXD signals and electronic flux densities are calculated using ORBKIT [66]. Mayavi [67] and Matplotlib [68] are used to visualize the electronic flux densities and the time-resolved x-ray signals, respectively.

### III. RESULTS AND DISCUSSION

Our starting point is a pair of oriented R- and S-enantiomers of epoxypropane. In recent years, it has become possible to orient chiral molecules in space. This has been demonstrated both theoretically and experimentally in Refs. [69-71]. Orientation can be achieved using either skewed-polarized pulses, a centrifuge, or a combination of a static field and linearly polarized pulse. The resulting orientation has the R- and S-enantiomers pointing in opposite directions along the chiral axis. As the molecules are fixed in their own frame of reference, everything in this work is described in the molecular frame, where $z$ defines the chiral axis.

As in previous work, oriented epoxypropane is exposed to a linearly polarized pump pulse of 10 fs pulse duration with $9.1 \times 10^{14}$ W/cm$^2$ peak intensity to initiate the charge migration dynamics. The pulse is polarized at 45° in the $yz$-plane of the molecular frame of reference and has a 160 nm wavelength with sine-squared envelope. As a result of the interaction between the pump pulse and epoxypropane, ultrafast charge migration is set into motion.

For the R-enantiomer, 32%, 7%, and 2% electronic populations are transferred by the end of the pump pulse from ground state to the 3rd, 4th and 5th excited electronic states, respectively. The rest of the population remains in the ground state, which is responsible for a dynamics on the attosecond timescale. On the other hand, the 3rd, 4th and 5th excited states are populated at 37%, 10% and 13%, respectively, while nearly 30% remains in the ground state for the S-enantiomer [72]. The reason behind different electronic populations in R- and S-enantiomer can be attributed to different temporal evolution of the magnitude and the phase of the Cartesian components of the total dipole moment, as discussed in Ref. [72]. Since the populations at the end of the pump pulse are different for both enantiomers, the field-free charge migration looks significantly different in both cases. This can be revealed by investigation of the transient flux densities.

The electronic flux densities accompanying the charge migration for both enantiomers are presented in Fig. 1. To avoid the fast oscillating contribution stemming from the coherent interaction with the ground state in the charge migration, only contributions from the excited states are considered in the reconstructed signal. Snapshots are presented for 2 fs, 6 fs, 10 fs, and 14 fs. The 2D representation in the $xz$-plane is obtained by integrating over the $y$ coordinate. The arrows of the vector field are color-coded according to their magnitude. In both enantiomers, almost all the flux density is concentrated around the oxygen atom (in maroon). It is important to mention that, maybe surprisingly, the chiral carbon atom is not involved in the dynamics, as revealed by the transient flux densities [72]. The most striking difference lies in the magnitude of the currents. The strength of the flux densities for the R-enantiomer is weak in comparison to that for the S-enantiomer during the charge migration. At all times, they both exhibit a similar circular pattern around the oxygen atom. The direction of the circular charge migration changes as the dynamics progresses.

Since the direction of the electron flow is more prominent for the S-enantiomer, as reflected in Fig. 1(b), it can therefore be more readily described. Arrows corresponding to the flux densities are emerging from the oxygen atom in all directions, corresponding to an approximately circular current density. Yet, the longest arrows in red represent the most probable direction for the flow of electrons, and these are changing with time. At 2 fs, arrows are mostly emerging in the positive $x$-direction and it is almost reversed in the next snapshot, i.e., at 6 fs. The flux densities for the S-enantiomer are along the same direction at 2 and 14 fs, which indicate the partial recurrence. Similar observations can be made for the circular component of the current density in the R-enantiomer, where the direction of the circular current is opposite to that of the S-enantiomer. In contrast, the
FIG. 1. Time-dependent electronic flux densities for (a) R- and (b) S-enantiomers of epoxypropane in the xz-plane at 2 fs, 6 fs, 10 fs, and 14 fs after the pump pulse. Violet, maroon and gray colors are representing carbon, oxygen and hydrogen atoms, respectively. Here, the z-axis is defined as the chiral axis in the molecular frame of reference.

The current component with the largest magnitude points in the same direction for both enantiomers at all times. A tentative explanation could be that the circular component stems from the phase transferred to the molecule by the laser field. This leads to opposite relative phases among the three excited states. On the other hand, the dominant component of the flux density could be associated with the response of the electron cloud in the electric field during the preparation phase. This electronic response behavior would then be inherited by the subsequent charge migration dynamics, explaining that both enantiomers react with the same phase.

The different timescale of the charge migration can be understood by analyzing the characteristic timescales involved in the system, i.e., \( \tau = \hbar / \Delta E \), where \( \Delta E \) is the energy difference between two eigenstates. The characteristic timescales corresponding to \( E_3 = 7.56 \text{ eV} \), \( E_4 = 7.73 \text{ eV} \), and \( E_5 = 7.84 \text{ eV} \) are \( \tau_{43} = 24.32 \text{ fs} \), \( \tau_{53} = 14.77 \text{ fs} \) and \( \tau_{54} = 37.59 \text{ fs} \). Different contributions of the excited states and their respective interference including these timescales are the reason for non-identical charge migration in the two excited enantiomers.

Time-resolved x-ray diffraction is a technique that can be used to image the dynamics of charge migration with atomic-scale spatiotemporal resolutions. In recent years, different formalisms of TRXD have been developed to image an increasing number of processes [42, 58, 59, 61, 73–78]. To simulate time-resolved diffraction signal, the DSP is computed according to Eq. (8). The six lowest-lying excited eigenstates (i.e., \( j = [0, 6] \)) were sufficient to obtain the converged diffraction signals under the assumption that the sum-over-states expression was truncated due to the detector response.

The time-independent contributions to the total diffraction signal for both enantiomers after the excitation are presented in Fig. 2. These signals are simulated using Eq. (8). From the figure, one can see that the time-independent diffraction signals are different for both enantiomers. First, the intensity of the time-independent signal is stronger for the R-enantiomer in comparison to the S-enantiomer. This is especially true in the low-
FIG. 3. Time-resolved diffraction patterns for (a) R- and, (b) S-enantiomers of epoxypropane in $Q_z - Q_x$ plane at 2 fs, 6 fs, 10 fs, and 14 fs. Intensity of the diffraction patterns is presented in units of $dP/d\Omega$. Here, time-dependent diffraction signal at $T = 0$ fs is subtracted to the subsequent delay time. An ultrashort x-ray pulse of 8 keV mean energy is aimed to obtain 1.55 Å spatial resolution in these simulations. All diffracted photons up to 60° are collected in the detector.

momentum region. Also, the signals are not mirror images of each other, which could allow one to discriminate between the enantiomers by simple inspection of the two diffraction signals. Since these diffraction signals are static in nature, the dynamical information about the charge migration is lost.

Time-resolved diffraction signals at selected delay times for both enantiomers are presented in Fig. 3. The total diffraction signal at $T = 0$ fs is subtracted from the signal at subsequent delay times. It is observed that the time-independent signal is three orders of magnitude stronger than this time-dependent signal. Similar observations have been reported earlier in the case of TRXD for different systems [45, 79]. In spite of having low magnitude, the information about the ultrafast dynamics of charge migration is imprinted in the different diffraction signals as they are significantly different for both enantiomers at different delay times. The central parts as well as the higher-momentum signals are changing in a very distinct way for both enantiomers. Note that $\langle \Phi_i|\Phi_j \rangle$ is not exactly zero in our case due to numerical limitations, which impose using a small but finite value with a threshold value of $10^{-5}$ on the linear-response TDDFT coefficients. This, together with the numerical coefficient renormalization, explains the small but non zero value of the diffraction signal at the center in Fig. 3.

By comparing the time-dependent diffraction pattern of the enantiomers at 2 fs, it can be seen that the overall signals are not very different for both enantiomers. There are two lobes of positive signal around the center and they are of almost the same intensity with different orientations for the respective enantiomers. The negative part of the signal is scattered at higher momenta. There is a mismatch in the intensity at the central part of the lobes for the two enantiomers.

At the next delay step, i.e., at 6 fs, the diffraction signal is reduced significantly for both enantiomers. The signal is just reversed around the center, dominated by a negative value and spreading to higher momenta for the S-enantiomer. For the R-enantiomer, the signal at 10 and 14 fs are similar to the one at 2 fs and reflect slower dynamics. In contrast, for the S-enantiomers, the signal at 10 fs is comparable to the signal at 2 fs but not identical due to the presence of four dips with a minimum value around the center. There is overall depletion of the signal at 14 fs compared to the previous time step. The oscillation period of the time-dependent signal correlates well with the timescale of the charge migration found in the flux density for the enantiomers as shown in Fig. 1.

In order to understand how the time-dependent diffraction signals are related to the flux density, the time derivative of the electron density in momentum space, $|\partial_t \rho(Q)|$, at selected delay times is presented in Fig. 4. At $T = 0$ fs, $|\partial_t \rho(Q)|$ is zero (see Eq. (S7) in Ref. [34]).
FIG. 4. Time derivative of electron density in momentum space, $|\partial_t \rho(Q)|$, for (a) R- and, b) S-enantiomers of epoxypropane in $Q_x - Q_z$ plane at 2 fs, 6 fs, 10 fs, and 14 fs.

Therefore, subtracting $|\partial_t \rho(Q)|$ at $T = 0$ fs is not required. The $|\partial_t \rho(Q)|$ is related to the flux densities, and it can be obtained by a Fourier transform of the electronic continuity equation, Eq. (4).

For both enantiomers, the overall signal of $|\partial_t \rho(Q)|$ decreases drastically from 2 fs to 6 fs. There is a partial revival of the signal at 10 fs for the R-enantiomer as observed in Figs. 1 and 3. The intensity of $|\partial_t \rho(Q)|$ at 14 fs increases compared to that in 10 fs for the R-enantiomer. In contrast, $|\partial_t \rho(Q)|$ for the S-enantiomer at 14 fs is approximately similar to the one at 2 fs.

As evident from Figs. 3 and 4, it is not straightforward to establish visual one-to-one correspondence between the DSP and $|\partial_t \rho(Q)|$, which is in contrast to the earlier work discussed in Ref. [34]. There are two simple reasons behind this. The first one is that more than two electronic states are contributing to the electronic wavepacket in epoxypropane. As a result, time-dependent terms yield more than one sine term in the expression of $|\partial_t \rho(Q)|$ (see Eq. (S7) in Ref. [34]). The other reason can be attributed to a significant contribution stemming from the sine square term in comparison to the sine term in the expression of $\Delta dP/d\Omega$ (see Eq. (S12) in Ref. [34]). These findings are in contrast to an earlier case, where the wavepacket was composed of only two electronic states, and the sine square term was negligibly small in comparison to the sin term [34]. Therefore, the comparison between the DSP and $|\partial_t \rho(Q)|$ can only be qualitative.

As the time-resolved diffraction signals for the two enantiomers are different, we can define the asymmetry parameter as

$$Y = \frac{\sigma_R - \sigma_S}{\sigma_R + \sigma_S},$$

where $\sigma_R$ and $\sigma_S$ are the DSPs of the R- and S-enantiomers, respectively. Here, the DSP is represented by $\sigma$ as an abbreviation. Figures 3(a) and 3(b) present, respectively, the asymmetry parameter along $Q_x$ and $Q_z$ axes, respectively, as a function of time. The domination of the red part over the blue is an indication that the signal for the S-enantiomer is stronger than that for the R-enantiomer along the $Q_x$ axis. If we look only around the $Q_x = 0$ line, the signal for the R-enantiomer is dominating over the S-enantiomer for all the time steps. The case is almost reversed for $Q_x \neq 0$.

The signals are more interesting along the chiral axis, i.e., along the $Q_z$ axis. For a specific point in momentum space, the signal is changing in a periodic fashion. The same is true if we fix the time-delay and walk along the $Q_z$ axis. These signals encode important information about the dynamical evolution of the system, which is unique for a given choice of laser tagging parameters.

The asymmetry parameter can be used to determine the enantiomeric ratio in a sample of unknown concentrations $C_R$ and $C_S$ in the R and S enantiomers, respectively. In this case, the measured signal of the unknown mixture is given as the weighted sum of the two signals $\sigma_{\text{sample}} = C_R \sigma_R + C_S \sigma_S$. By subtracting from the TRXD...
FIG. 5. Asymmetry parameter $Y$ along the (a) $Q_x$ and, (b) $Q_z$ axes as a function of the delay time. The 1D TRXD signal is obtained from Eq. (7) and integrated along the other axes.

signal of a pure enantiomer, say, $\sigma_R$, this difference

$$\Delta \sigma = \sigma_R - (C_R \sigma_R + C_S \sigma_S)$$
$$= (1 - C_R)\sigma_R - C_S \sigma_S = C_S (\sigma_R - \sigma_S) \quad (10)$$

can be simply normalized and related to the asymmetry parameter

$$\frac{\Delta \sigma}{\sigma_R + \sigma_S} = C_S \left( \frac{\sigma_R - \sigma_S}{\sigma_R + \sigma_S} \right) = C_S Y, \quad (11)$$

Hence, from the knowledge of the TRXD signals of both enantiomers, the concentration of an enantiomer can be directly obtained by comparing the intensity of the difference signal with that of the asymmetry parameter. As the dynamics becomes more intricate at longer times, the time-dependent monitoring of the different signals would potentially lead to a more precise determination of the concentrations.

### IV. CONCLUSION

The present work aimed at imaging the charge migration in epoxypropane using TRXD. The charge migration in oriented epoxypropane was triggered by a linearly polarized pulse at 45° in the $yz$-plane in the molecular frame of reference. For each enantiomer, the induced charge migration was different, and is imaged by TRXD. The dominating time-independent and different TRXD signals were analyzed separately. It was found that time-dependent diffraction signals are significantly different for both enantiomers. We believe that the present proof-of-principle results should motivate further studies of laser-induced charge migration in chiral molecules imaged by TRXD. In particular, this could pave the way for a new, sensitive technique to determine the enantiomeric concentrations in unknown samples.

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