JET PRODUCTION AT HERA AND MEASUREMENTS OF THE STRONG COUPLING CONSTANT $\alpha_s$

DORIAN KCIRA

University of Wisconsin
ZEUS / DESY, Notkestrasse 85, 22607 Hamburg, Germany
Email: dorian.kcira@desy.de

Measurements of HERA that explore the parton dynamics at low Bjorken $x$ are presented together with precise determinations of the strong coupling constant $\alpha_s$. Calculations at next to leading order using the DGLAP evolution fail to describe the data at low $x$ and forward jet pseudorapidities. The $\alpha_s(M_Z)$ measurements at HERA are in agreement with the world average and have very competitive errors.

1. Introduction

At HERA, forward jet production and jet-jet correlations are expected to be sensitive to the parton dynamics at low Bjorken $x$ ($x_{Bj}$). In the first section, these type of measurements and comparison to DGLAP, BFKL and other models are presented. For the measurements presented in the second section, jets were selected in kinematic regions where the proton parton distribution functions (PDFs) are well constrained and the DGLAP equations are valid. These measurements allow precise tests of perturbative QCD (pQCD) and the determination of the strong coupling constant, $\alpha_s$.

2. QCD dynamics at low $x$

Inclusive forward jet production was measured by the H1 Collaboration \(^1\) for events in the kinematic region $5 < Q^2 < 85$ GeV\(^2\) and $10^{-4} < x_{Bj} < 4 \cdot 10^{-3}$, where $Q^2$ is the virtuality of the exchanged photon. Jets were found in the laboratory frame with $E_T^{\text{jet}} > 3.5$ GeV, $7^\circ < \theta_{\text{jet}} < 20^\circ$ (corresponding to the $1.74 < \eta^{\text{jet}} < 2.8$ \(^a\)), $x_{\text{jet}} > 0.035$, and $0.5 < E_T^{\text{jet}}/Q^2 < 5$. $E_T^{\text{jet}}$ is the transverse energy of the jet and $x_{\text{jet}}$ is the fractional energy of the proton taken by the jet.

\(^a\eta = -\log[\tan(\theta/2)]\) is the pseudorapidity, where $\theta$ is the polar angle.
The measured cross section is shown in Fig. 1 as a function of $x_{Bj}$ and compared to the prediction of NLO calculations from DISENT (left) and various QCD models (middle). The DISENT calculations were performed using the CTEQ6M parametrization of the proton PDFs. The renormalization scale was chosen to be $\mu_R = E_{T}^{jet}$. The DGLAP model with direct photon interactions alone (RG-DIR, RAPGAP) and the NLO calculation fall below the data, especially at low $x_{Bj}$. The description of the data by RAPGAP is significantly improved if contributions from resolved photon interactions are included (RG-DIR+RES). The Color Dipole Model (CDM) shows a similar behaviour to RG-DIR+RES. In addition, the CCFM based CASCADE MC predicts a different shape of the distribution that results in a poor description of the data.

Jet production in NC DIS has been measured by the ZEUS Collaboration for $Q^2 > 25$ GeV$^2$, $y > 0.004$, $E'_e > 10$ GeV (where $E'_e$ is the energy of the scattered positron), and $\cos(\gamma_h) < 0$. Jets were selected in the laboratory frame with $E_{T}^{jet} > 6$ GeV, $2 < \eta^{jet} < 3$, and $0.5 < (E_{T}^{jet})^2/Q^2 < 2$.

The measurement is presented in Fig. 1 (right) as a function of $x_{Bj}$ and compared to NLO calculations (DISENT, $\mu_R = \mu_F = Q$, CTEQ6) and to the CDM (ARIADNE) and MEPS (Matrix Elements + Parton Showers, LEPTO) models. The CDM prediction gives a reasonable description of the data.

---

$\gamma_h$ is the hadronic angle. It corresponds, in the Quark Parton Model, to the angle of the scattered quark.
data. The NLO and MEPS predictions fail to describe the data in the low $x_{\text{Bj}}$ region. The uncertainty induced by the variation of the renormalization scale is large, indicating that missing higher order or $\ln(1/x)$ terms in the calculation could be important in this region.

The H1 Collaboration has measured inclusive dijet production in DIS \(^3\) in the kinematic range $5 < Q^2 < 100$ GeV\(^2\), $10^{-4} < x < 10^{-2}$, and $0.1 < y < 0.7$. Dijets were reconstructed in the hadronic center-of-mass system (HCM) and selected with the requirements: $-1 < \eta_{\text{jet},\text{lab}} < 2.5$ and $(E_{\text{jet}}^{1,2})^* > 7.5$ GeV. The azimuthal asymmetry is defined by: $S(\alpha) = \frac{\int_{\alpha}^{\beta} N_{\text{dijet}}(\Delta \phi^*, x, Q^2) d\Delta \phi^*}{\int_{\alpha}^{\beta} N_{\text{dijet}}(\Delta \phi^*, x, Q^2) d\Delta \phi^*}$, where $\Delta \phi^*$ is the azimuthal separation in the HCM frame between the two hardest transverse energy jets.

Figure 2 presents the $S$ distribution for $\alpha = 120^\circ$ as a function of $x$ for different $Q^2$ compared to predictions of DGLAP NLO calculations (left) and different models (right). The measured values of $S$ for the chosen $\alpha$ are of the order of 5% and increase with decreasing $x$. The rise is most prominent in the lowest $Q^2$ bin. The DISET (\(\mathcal{O}(\alpha_2^2)\)) calculations predict no rise of $S$ with $x$ and fall below the measurements. The NLOJET (\(\mathcal{O}(\alpha_3^3)\)) give a good description of the data at large $Q^2$ and large $x$ but fail to describe the strong rise towards low $x$, particularly in the lowest $Q^2$ range. A good description of the $S$ distribution at low $x$ and low $Q^2$ is predicted from the CDM model. The CCFM based CASCADE predictions depend strongly on the choice of the unintegrated gluon density.

![Figure 2](image)

Figure 2. Azimuthal asymmetry $S$ for $\Delta \phi^* < 120^\circ$ as a function of $x_{\text{Bj}}$ and $Q^2$. The data are compared to NLO predictions (left) and to the CCFM and CDM models (right).
3. Precise tests of QCD and the measurement of $\alpha_s$

Differential dijet and trijet cross sections have been measured by the ZEUS Collaboration\(^4\) in the kinematic range $10 < Q^2 < 5000$ GeV\(^2\) and $0.04 < y < 0.6$. Jets were found in the Breit frame and dijet (trijet) events were selected with: $-1 < \eta_{\text{jet,lab}} < 2.5$, $E_{\text{T,jet,Breit}} > 5$ GeV, and invariant mass $M_{2/3\text{jets}} > 25$ GeV.

Figure 3 shows the measured dijet and trijet cross sections as a function of $Q^2$ (left) and their measured ratio $R_{3/2}$ (middle). The NLO predictions of NLOJET ($\mu_R = \mu_F = (E_T^2 + Q^2)/4$, CTEQ6) corrected for hadronization effects are compared to the data. NLOJET provides a good description of both the shape and the magnitude of the measured cross section. The correlated systematic and the renormalization scale uncertainties largely cancel in the ratio of the cross sections. This cancellation allows the extraction of $\alpha_s(M_Z)$ with a good precision down to $Q^2$ of $10$ GeV\(^2\), using a method similar to that of a previous ZEUS publication\(^5\). The value of $\alpha_s$ was measured to be $\alpha_s(M_Z) = 0.1179 \pm 0.0013$ (stat.) $^{+0.0028}_{-0.0046}$ (exp.) $^{+0.0064}_{-0.0046}$ (th.).

Figure 4. A summary of the $\alpha_s$ from measurements at HERA.
Jet substructure for jets produced in DIS has been measured by the ZEUS Collaboration\footnote{ZEUS Collab., DESY-05-019 (2005)} for $Q^2 > 125$ GeV$^2$. Jets were reconstructed in the laboratory frame and were selected with $E_T^{\text{jet}} > 17$ GeV and $-1 < \eta^{\text{jet}} < 2.5$. The mean integrated jet shape is defined as the averaged fraction of the jet transverse energy inside the cone of radius $r$: 
$$
\langle \psi(r) \rangle = \frac{1}{N_{\text{jets}}} \sum_{\text{jets}} \frac{E_T(r)}{E_T^{\text{jet}}},
$$
where $E_T^{\text{jet}}$ is the total transverse energy of the jet, $E_T(r)$ the part of it inside the cone of radius $r$ and $N_{\text{jets}}$ is the total number of jets in the sample.

Figure 3 (right) shows the measured $\langle \psi(r = 0.5) \rangle$ as a function of $\eta^{\text{jet}}$ and $E_T^{\text{jet}}$. There is no significant variation of $\langle \psi(r = 0.5) \rangle$ with $\eta^{\text{jet}}$ in DIS, whereas $\langle \psi(r = 0.5) \rangle$ increases as $E_T^{\text{jet}}$ increases. The sensitivity of the measurements to the value of $\alpha_s(M_Z)$ is illustrated in Fig. 3 (lower part of plot) by comparing the measured $\langle \psi(r = 0.5) \rangle$ to NLO QCD calculations using three different values of $\alpha_s(M_Z)$. The NLO QCD calculations provide a good description of the measured $\langle \psi(r = 0.5) \rangle$ and thus this observable was used to determine $\alpha_s(M_Z)$. The value of $\alpha_s(M_Z)$ as determined by fitting the NLO QCD calculations to the measured mean integrated jet shape $\langle \psi(r = 0.5) \rangle$ for $E_T^{\text{jet}} > 21$ GeV is $\alpha_s(M_Z) = 0.1176 \pm 0.0009$ (stat.) $^{+0.0009}_{-0.0026}$ (exp.) $^{+0.0091}_{-0.0072}$ (th.).

4. Conclusions

The HERA measurements show that DGLAP NLO calculations at low $x$ and forward jet pseudorapidities fail to describe data but the large theoretical uncertainties prevent a decisive conclusion on parton dynamics at low $x$. A summary of the $\alpha_s$ measurements at HERA is shown in Fig. 4. The $\alpha_s$ measurements at HERA are in agreement with the world average and have very competitive errors. For more accurate measurements of $\alpha_s$ improved theoretical calculations would be needed.

References
1. H1 Collab., Contributed Paper N 5-0172 to 32nd ICHEP, Beijing, 2004
2. ZEUS Collab., DESY-05-017 (2005)
3. H1 Collab., A. Aktas et al., Eur. Phys. J. C37 141 (2004)
4. ZEUS Collab., DESY-05-019 (2005)
5. ZEUS Collab., Phys. Lett. B 507, 70 (2001)
6. ZEUS Collab., Nucl. Phys. B 700, 3 (2004)