Assessment of Wastewater Treatment Plant Performance using Capability Indices

Estimating Capability of Wastewater Treatment Processes

Kailas Govinda Khadse
Department of Statistics,
Moolji Jaittha College,
Jalgaon, India

Aditya Kailas Khadse
Digitate,
Tata Consultancy Services Ltd,
Pune, India

Abstract — In usual practice, performance of wastewater treatment plant is assessed by percentage removal of Chemical Oxygen Demand (COD), Biochemical Oxygen Demand (BOD) and Total Suspended Solids (TSS) from wastewater after processing. Besides these, while measuring performance of wastewater plant environmental engineers also expect to consider the status of characteristics such as pH, NH\textsubscript{3}-N, N-Total, fecal coliform, etc at outlet. The problem with usual practice of performance assessment is that there is no direct comparison between these characteristics process distribution at outlet stage and effluent discharged standards or specification limits developed by Central Pollution Control Board (CPCB) for these characteristics. Considering this lacuna in mind, in this paper we propose and use probability based Process Capability Indices (PCIs) and Multivariate Process Capability Indices (MPCIs) which compares the output of wastewater treatment process with the process specifications and quantify how well the process performs. PCIs have been widely used in evaluating the performance of manufacturing processes and used as a basis to improve the process performance. From an environmental engineer’s point of view, the intention of this paper is to extend applications of PCIs and MPCIs in the field of environmental engineering. Measuring wastewater treatment process performance using capability indices effectively and then process improvement based on these indices is necessary to save the environment and enable reuse of processed water. The wastewater treatment process capability analysis using appropriate capability indices is presented in the paper based on secondary data which is collected from case studies through literature survey. It is found that using appropriate capability indices, wastewater treatment processes performance can be assessed effectively as compared to usual practice.

Keywords— Process capability indices; process distribution; process variation; normal distribution; wastewater treatment plant capability; effluent discharged standards; wastewater treatment process; multivariate normal distribution.

I. INTRODUCTION

As compared to developed countries, there is sizeable gap in untreated wastewater and treated wastewater at India level [1]. Untreated wastewater and low quality of treated wastewater contaminate the environment. In view of this issue, there is an urgent need to increase the number of best performing wastewater treatment plants with huge capacity and to improve the performance of existing wastewater treatment plants. Enhancing the quality status of treated wastewater will save the environment and water crisis problem would be solved up to certain level by reusing this water. Process capability analysis using appropriate capability indices is the base to improve the wastewater treatment process performance. Process capability analysis with capability indices uses statistical tools to know how well a process performs with reference to process characteristics standards or specification limits. Wastewater treatment process capability analysis with capability indices considers the definition of quality which is based on the viewpoint that wastewater treatment process must meet specified requirements regarding effluent discharged set by Central Pollution Control Board (CPCB) [2].

In usual practice performance of wastewater treatment plant is assessed by percentage removal of Chemical Oxygen Demand (COD), Biochemical Oxygen Demand (BOD) and Total Suspended Solids (TSS) from wastewater after processing. Besides these environmental engineer also expects to consider the status of characteristics such as pH, NH\textsubscript{3}-N, N-Total, fecal coliform etc at outlet while measuring process performance. There are number of research articles where wastewater treatment plant performance is measured through percentage removal of BOD, TSS etc. [3, 4, 5, 6, 7 and 8]. Evaluated performance of wastewater treatment plant with Activated Sludge Method was measured and noted as removal efficiency of BOD is 94.56% and removal efficiency of TSS is 93.72% [3]. Evaluated performance of wastewater treatment plant was measured as COD removal efficiency is 69.39% and BOD removal efficiency is 62.78% [5]. Indian standards with regard to effluent discharged for wastewater treatment plant, in case of characteristic BOD (mg/l) is “not more than 10” and for COD (mg/l) is “not more than 50” [2]. Formula of removal efficiency of BOD considers BOD at inlet stage and BOD at outlet stage. On similar lines formula of removal efficiency of COD considers BOD at inlet stage and BOD at outlet stage. These formulae do not consider specification limits for these characteristics while measuring performance of wastewater treatment plant. So the problem with usual practice of performance assessment is that there is no direct comparison between wastewater treatment process characteristics distribution at outlet stage and effluent discharged standards or specification limits developed by CPCB for these characteristics. Considering this lacuna in mind, in this paper we propose and use capability indices which compares the output of wastewater treatment process with the process specifications and quantify how well the process performance.

The study of univariate process capability analysis began as a comparison of the stable process distribution with product specification in the form of lower and upper specification limits. Initially the judgment of process capability was based on histogram which is one of the important statistical process

IJERTV9IS040267 www.ijert.org

(This work is licensed under a Creative Commons Attribution 4.0 International License.)

267
control tool. Considering the limitations of histogram tool to assess capability, there was quick demand of process capability measure from practitioners. Thus the PCI was born as a measure of process capability. PCIs have been extensively studied in the literature with their estimators, distributional and inferential properties [9, 10]. PCIs have been widely used in evaluating the quality performance of manufacturing processes; they can be effectively used to evaluate environmental performance [11, 12]. In real life situations, many processes are multivariate in nature. Considering the issue of multivariate process in mind, multivariate process capability indices (MPCIs) were developed as measures to measure multivariate process capability during the last three decades [13, 14, 15]. MPCIs are based on multivariate statistical methods and they consider the variables jointly with their correlation structure. PCIs as well as MPCIs were recently reviewed and strengths and weaknesses of each index were discussed[16].

The structure of this article is as follows. In section 2, we discuss basic PCIs and their assumptions with their proposed probability based alternative forms. This section also extends definition of probability based PCIs in multivariate setup. From environmental engineer’s point of view, section 3 deals with two case studies taken from literature and then wastewater treatment plant capability analysis with their proposed estimators. Here we discuss basic PCIs and their assumptions with their proposed alternative forms of CPU and CPL. Assuming assumptions as mentioned in the beginning of section II, we define alternative form of CPU and CPL [14]. Assuming assumptions as mentioned in the beginning of section II, we define alternative form of CPU and CPL [14].

### II. PCIS AND MPCIS TO MEASURE ACTUAL PROCESS PERFORMANCE

#### A. Univariate traditional PCIs

PCIs CPU and CPL are defined under the assumptions that:

1) the process is in statistical control
2) a tolerance region of a quality characteristic is specified by lower or upper specification limits (LSL or USL) and
3) the process measurement (X) are normally distributed with mean \( \mu \) and variance \( \sigma^2 \). The probability density function of normal distribution having mean \( \mu \) and variance \( \sigma^2 \) is given below.

\[
f(x; \mu, \sigma) = \frac{1}{\sigma \sqrt{2\pi}} e^{\frac{-1}{2} \left(\frac{x - \mu}{\sigma}\right)^2}, \quad -\infty < x, \mu < \infty, \quad \sigma > 0
\]

The Upper (CPU) and Lower (CPL) Capability Indices are defined as

For a given USL, the upper capability index is given by

\[
CPU = \frac{USL - \mu}{3\sigma} \quad (1)
\]

Similarly for given LSL, the lower capability index is given by

\[
CPL = \frac{\mu - LSL}{3\sigma} \quad (2)
\]

If a tolerance region of quality characteristic is specified by LSL and USL then most frequently used capability index is \( C_{pk} \), which is defined by \( \min(\text{CPU}, \text{CPL}) \).

**Capability requirement:** A process is called not capable if capability index is less than one; it indicates process is not capable with respect to specifications; in such a situation process standard deviation (\( \sigma \)) needs to be reduced and/or process mean (\( \mu \)) to be adjusted. A process is called capable if capability index is greater than or equal to 1. Magnitude of capability index value gives us the answer of question how well the process performance with respect to standards or specifications. Process performance status is satisfactory if capability index is lies between (1.33, 1.50) and is said to be excellent if it is greater than 1.5.

In practice parameters \( \mu \) and \( \sigma \) are replaced by their estimators \( \hat{\mu} \) and \( \hat{\sigma} \) computed from sample \( X_1, X_2, ..., X_n \).

That is

\[
\hat{\mu} = \bar{X} = \frac{1}{n} \sum_{i=1}^{n} X_i, \quad \text{and}
\]

\[
\hat{\sigma} = S = \sqrt{\frac{1}{n-1} \sum_{i=1}^{n} (X_i - \bar{X})^2}.
\]

#### B. Probability based PCIs to measure process performance

In view of various problems of constructing capability indices for univariate as well as multivariate set up, probability based PCI are very useful as compared to traditional PCIs as well as MPCIs [14]. Assuming assumptions as mentioned in the beginning of section II, we define alternative form of CPU and CPL as given below. These alternative forms are smooth version of CPU and CPL.

\[
CPU_{(p)} = -\frac{1}{3} \Phi^{-1} \left(\frac{1-p}{2}\right); \quad \text{where} \quad p = P(X < \text{USL} | \mu, \sigma^2)
\]

\[
CPL_{(p)} = -\frac{1}{3} \Phi^{-1} \left(\frac{1-p}{2}\right); \quad \text{where} \quad p = P(X > \text{LSL} | \mu, \sigma^2)
\]

Here \( \Phi^{-1} \) denotes the inverse distribution function of the standard normal distribution. PCIs \( CPU_{(p)} \) and \( CPL_{(p)} \) estimated using \( \hat{p} \) by replacing \( \mu \) and \( \sigma \) by their estimators \( \hat{\mu} \) and \( \hat{\sigma} \).

**Remark 1:** If a tolerance region of quality characteristic is specified by LSL and USL then alternative form of \( C_{pk} \) is defined as given below.

\[
C_{pk(p)} = -\frac{1}{3} \Phi^{-1} \left(\frac{1-p}{2}\right); \quad \text{where} \quad p = P(\text{LSL} < X < \text{USL} | \mu, \sigma^2).
\]

**Remark 2:** Range of random variable in normal distribution is \(-\infty \) to \( \infty \); and using the property of probability density function \( P(-\infty < X < \infty) = 1 \). But some times for highly capable processes, due to computational limitation it may happen that \( p \) defined in “(3)” and “(4)” and remark 1 comes out to be 1; in that case take \( p \) to be just less than one, say \( p=0.99999999 \).
C. Probability based MPCIs to measure process performance

We define multivariate version of CPU\(_p\) and CPL\(_p\), as an alternative to multivariate analogue of CPU and CPL respectively denoting by MCPU\(_p\) and MCPP\(_p\). These MPCIs are defined under the assumption that

1) only a single specification limit is given for each quality characteristics
2) the process is in statistical control
3) denoting the \(i^{th}\) \((i=1,2,…,m)\) quality characteristics by \(X_i\), the process distribution of \(X = (X_1, X_2, …, X_m)\) is multivariate normal with mean vector \(\mu\) and variance covariance matrix is \(\Sigma\). An m-dimensional normal density for the random vector \(X\) has the form is given below.

\[
f(x) = \frac{1}{\left(2\pi\right)^{\frac{m}{2}}\left|\Sigma\right|^\frac{1}{2}} e^{-\frac{1}{2}(x-\mu)^'\Sigma^{-1}(x-\mu)}
\]

\(-\infty < x_i, \mu_i < \infty; \quad (i = 1, 2, …, m)\)

and \(\Sigma\) is positive definite matrix.

Alternative multivariate version for CPU and CPL are given below.

\[
\text{MCPU}_{p(i)} = \frac{1}{\Phi} \Phi \left[ \frac{1 - p}{2} \right] ; \quad \text{for} \quad p = P(X < \text{USL}|\mu, \Sigma) \tag{5}
\]

\[
\text{MCPL}_{p(i)} = \frac{1}{\Phi} \Phi \left[ \frac{1 - p}{2} \right] ; \quad \text{for} \quad p = P(X > \text{LSL}|\mu, \Sigma) \tag{6}
\]

Here \(\Phi^{-1}\) denotes the inverse distribution function of the standard normal distribution. These MPCIs estimated using \(\hat{p}\) by replacing \(\mu\) and \(\Sigma\) by their estimators which are sample mean vector and sample variance covariance matrix.

III. CASE STUDIES WITH CAPABILITY ANALYSIS

The wastewater treatment process capability analysis presented which is based on secondary data taken from case study 1 [17] and case study 2 [7].

A. Case Study 1

Description with data: This study evaluates the performance efficiency of wastewater plant operating on biological treatment method with an average wastewater inflow of 6 MLD. This plant is located at Sector-8, Charkop, Mumbai, Maharashtra, India. This case study dataset contains nine biweekly (Oct 2018-May 2019) measurements of BOD in mg/l, COD in mg/l and TSS in mg/l at four stages including inlet stage and outlet stage. For process capability analysis we have considered only outlet stage data. In statistical language, to analyze process capability, number of variables: 3 and number of observation per variable: \(n=9\). Dataset is given in Table 1.

| Sample | BOD in mg/l | COD in mg/l | TSS in mg/l |
|--------|-------------|-------------|-------------|
| 1      | 6.35        | 25          | 40          |
| 2      | 6.8         | 18.8        | 20          |
| 3      | 8.09        | 112.8       | 40          |
| 4      | 8.1         | 28.8        | 25          |
| 5      | 11.2        | 47          | 35          |
| 6      | 5           | 16.1        | 48          |

Table 1. BOD, COD AND TSS AT OUTLET FROM CASE STUDY 1

Capability analysis: While measuring wastewater treatment process capability using PCLs and MPCIs here we take following effluent standards for wastewater treatment plant developed by CPCB [2].

| Characteristic | Characteristic Limit (Not more than) |
|---------------|-------------------------------------|
| BOD (mg/l)    | 10                                  |
| COD (mg/l)    | 50                                  |
| TSS (mg/l)    | 20                                  |

Table II. EFFLUENT DISCHARGED STANDARDS FOR WASTEWATER TREATMENT PLANT

Step 1: Data is tested for outlier using Grubbs’ Test and following outliers are found at 5% significance level.

| Variable | Sample no. | Outlier |
|----------|------------|---------|
| BOD      | 5          | 11.2    |
| COD      | 3          | 11.2    |

So from further analysis sample number 3 and sample number 5 excluded from the data set.

Step 2: Data is tested for multivariate normality. Based on Royston’s H test it is found that data come from a multivariate normal distribution cannot be rejected at the 5% significance level because observed level of significance (P-Value) is 0.8822.

From this we conclude that \(X=(BOD, COD, TSS)\) follows multivariate normal distribution and variables BOD, COD and TSS follows normal distribution.

To get rough idea about process capability with respect to BOD, a visual presentation of distribution of BOD having estimated mean=6.8214 and Standard deviation=1.0566 is shown below in “Fig. 1”. Here USL for BOD is not more than 10. Almost all observations are below 10.
Step 4: Probability based MPCI is estimated using “(5)”, estimated value with estimation procedure is given below.

\[
\hat{\mu} = 20.8429 \quad \text{and} \quad 27.2857
\]

\[
\hat{\Sigma} = \begin{bmatrix} 1.1165 & 3.2439 & -6.2321 \\ 3.2439 & 24.3928 & 11.4690 \\ -6.2321 & 11.4690 & 182.9047 \end{bmatrix}
\]

\[
\hat{p} = P(X < (10,50, 20))=0.293917. \text{ This probability is computed using R software with package mvtnorm. M}_{CPU(p)} = 0.1257.
\]

Step 5: In step four we have noted point estimate of MCPU(p), we can estimate lower and upper limit of 95% confidence interval of MCPU(p) using simulation technique. To estimate interval estimate with 95% confidence coefficient, generate 5000 samples from predicted multivariate normal distribution with size 7. From each generated sample estimate p and then MCPU(p) following step 4 and in this way we get 5000 point estimates of MCPU(p). Compute 2.5th and 97.5th percentile of estimated MCPU(p). The 2.5th and 97.5th percentile of estimated MCPU(p) is the lower and upper bound of confidence interval of MCPU(p).

Following step 5, 95% confidence interval of MCPU(p) is (0.0160, 0.2724).

**Interpretation:** Here wastewater treatment plant is not capable to meet the effluent discharged standards for wastewater treatment Plant developed by CPCB. Because estimated values of MPCI; MCPU(p) is too less as compare to desirable value 1. This is also observed through 95% confidence interval of MCPU(p). In view of univariate process capability, process is capable with respect to BOD and COD; but process is not capable with respect to TSS. This statement is based on values of CPU(p) for these variables. To improve process capability we need to improve process capability with respect to variable TSS. Root cause analysis is needed to identify root causes of low capability with respect to variable TSS.

B. Case Study 2

**Description with data:** This study evaluates the performance efficiency of wastewater plant operating on Sequence Batch Reactor (SBR) technology with an average wastewater inflow of 10 MLD (million liters per day). Wastewater treatment plant is located near Gadli village in Kaithal town, Haryana, India. This case study dataset contains four to five observations per month, data was collected during Jan 2014 to April 2014. Data collected on nine Physical and Chemical parameters of plant at inlet stage and outlet stage which includes BOD in mg/l, COD mg/l and TSS in mg/l. For process capability analysis and to compare process capability of this plant with respect to process capability of case study 1 plant, we have considered only outlet stage data of BOD, COD and TSS. So in statistical language, to analyze process capability, number of variables: 3 and number of observations per variable: n=17. Dataset is given in Table 7.

**Capability analysis:**

**Step 1:** Data is tested for outlier using Grubbs’ Test and it is found that no outlier at the 5% significance level.

**Step 2:** Data is tested for multivariate normality. Based on Royston’s H test it is found that data come from a multivariate normal distribution cannot be rejected at the 5% significance level because observed level of significance (P-value) is 0.3212.

From this we conclude that \( X = \{BOD, COD, TSS\} \) follows multivariate normal distribution and variables BOD, COD and TSS follows normal distribution.

**TABLE V. SAMPLE CORRELATION MATRIX**

| Variable | BOD  | COD  | TSS  |
|----------|------|------|------|
| BOD      | 1.0  | 0.6215 | -0.4361 |
| COD      | 0.6215 | 1.0 | 0.1717 |
| TSS      | -0.4361 | 0.1717 | 1.0 |

**TABLE VI. ESTIMATED PROBABILITY BASED PCIS**

| Variable | \( \hat{\mu} \) | \( \hat{\Sigma} \) | CPU(p) |
|----------|-----------------|-----------------|--------|
| BOD      | 20.8429         | 27.2857         |        |
| COD      | 3.2439          | 24.3928         |        |
| TSS      | -6.2321         | 11.4690         |        |

**TABLE VII. BOD, COD AND TSS AT OUTLET FROM CASE STUDY**

| Sampling date | BOD (mg/l) | COD (mg/l) | TSS (mg/l) |
|---------------|------------|------------|------------|
| 03/01/14      | 06         | 29.12      | 07         |
| 11/01/14      | 06         | 32.12      | 10         |
| 17/01/14      | 08         | 29.2       | 12         |
| 24/01/14      | 07         | 22.12      | 08         |
| 30/01/14      | 08         | 27.12      | 08         |
| 05/02/14      | 09         | 36         | 12         |
| 12/02/14      | 12         | 37         | 12         |
| 18/02/14      | 09         | 38         | 12         |
| 23/02/14      | 11         | 40.12      | 13         |
| 28/02/14      | 10         | 25         | 12         |
| 06/03/14      | 08         | 49         | 12         |
| 10/03/14      | 06         | 37.12      | 13         |
| 14/03/14      | 10         | 26.0       | 14         |
| 19/03/14      | 07         | 32.57      | 14         |
| 24/03/14      | 09         | 29.13      | 15         |
| 30/03/14      | 12         | 31.12      | 16         |
| 06/04/14      | 10         | 48.28      | 20         |

**TABLE VIII. SAMPLE MEAN AND STANDARD DEVIATION**

| Variable | Mean | Standard deviation |
|----------|------|--------------------|
| BOD      | 8.7058 | 1.9610             |
| COD      | 33.4718 | 7.5757             |
| TSS      | 12.3529 | 3.1412             |

**TABLE IX. SAMPLE CORRELATION MATRIX**

| Variable | BOD  | COD  | TSS  |
|----------|------|------|------|
| BOD      | 1.0  | 0.1744 | 0.5252 |
| COD      | 0.1744 | 1.0 | 0.4854 |
| TSS      | 0.5252 | 0.4854 | 1.0 |
To improve process capability we need to improve process capability with respect to all variables. This statement is based on values of $\hat{\mu}$, $\hat{\sigma}$, and estimated MPCI; $MCP_u(p)$ is too less as compare to needed to identify root causes of low capability with respect to all variables.

$\hat{\mu} = \begin{bmatrix} 8.7058 \\ 33.4717 \\ 12.3529 \end{bmatrix}$ and $\hat{\Sigma} = \begin{bmatrix} 3.8455 & 2.5911 & 3.2352 \\ 2.5911 & 57.3923 & 11.5537 \\ 3.2352 & 11.5537 & 9.8676 \end{bmatrix}$

$\hat{p} = P(X < (10,50,20))\approx 0.7357307$. This probability is computed using R software with package mvtnorm. $MCP_u(p) = 0.3721$.

Step 5: To estimate interval estimate with 95% confidence coefficient, generate 5000 samples from predicted multivariate normal distribution with size 17. Remaining procedure is same as explained in step 5 of case study 1. 95% confidence interval of $MCP_u(p)$ is $(0.2592, 0.5452)$.

A visual presentation of histogram of estimator of $MCP_u(p)$ is given below in “Fig. 2”. This will help us if needed to study properties of estimator.

**TABLE X. ESTIMATED PROBABILITY BASED PCIS**

| Variable | $\hat{p} = P(X < USL \mid \hat{\mu}, \hat{\sigma})$ | $MCP_u(p)$ |
|----------|--------------------------------------------------|-------------|
| BOD      | 0.7453633                                        | 0.3797      |
| COD      | 0.9854356                                        | 0.8143      |
| TSS      | 0.9925428                                        | 0.8919      |

**IV. CONCLUSION**

The problem with usual practice of assessment of performance of wastewater treatment plant is that there is no direct comparison between wastewater treatment process distribution at outlet stage and effluent discharged standards or specification limits developed by CPCB. Considering this lacuna in mind, in this paper we have defined and used probability based PCIs and MPCIs which compares the output of wastewater treatment process with the process specifications and quantify how well the process performance. Capability indices have been widely used in evaluating the quality performance of manufacturing processes; it is found that they can be effectively used to evaluate the performance of wastewater treatment plant. We have studied two wastewater treatment plants through capability analysis and defined probability based PCIs and MPCIs. Both plants processes not capable to meet the standards developed by CPCB. Though both plants are not capable to meet the standards but wastewater treatment plant located near Gadli village in Kaithal town, Haryana, India is a little bit more capable as compared to other plant which is located at Sector-8, Charkop, Mumbai, Maharashtra, India because former plant estimated MPCI is large as compared to latter. This is also observed through comparing confidence interval of respective plants MPCIs. To improve capability of these plants, root cause analysis is needed to identify root causes of low capability. Though we have assumed multivariate normal process we can extend definitions of probability based PCIs and MPCIs when distribution of process is not multivariate normal because our definitions base is conforming probability. To get good estimate of PCIs or MPCIs in accuracy and precision point of view, large sample is needed.

**REFERENCES**

[1] Gautam S. K., Sharma D., Tripathi J. K., Ahirwar S. and Singh S. K. “A study of the effectiveness of sewage treatment plants in Delhi region”, Applied Water Science, vol. 3(1), pp. 57–65, 2013
[2] CPCB Environmental Information System “Newsletter on Control of Pollution”, Issue 1, 2015
[3] K. S. Kumar, P. S. Kumar and M. J. Ratnakanth Babu “Performance evaluation of wastewater treatment plant”, International Journal of Engineering Science and Technology, Vol. (2012), pp. 7785-7796, 2010
[4] Coskuner, G. and Ozdemir, N. “Performance assessment of a wastewater treatment plant treating weak campus wastewater”, International Journal of Environment and Pollution, Vol. 28(1/2), pp. 185-197, 2006
[5] G. Chandrakant, P. Jaswanth, S.Teja reddy, and G. Kiranmai “Design & performance evaluation of wastewater treatment plant-D at Tirumala”, International Journal of Scientific & Engineering Research, Vol. 6(7), pp. 1672-1688, 2015
[6] P. N. Wakode, and S. U. Sayyad “Performance evaluation of 25MLD sewage treatment plant (STP) at Kalyan”, American Journal of Engineering Research, Vol. 3(3), pp. 310-316, 2014
[7] A. Pipraiya “Performance evaluation of wastewater treatment plant based on SBR technology- A case study of Kaithal town, Haryana (India)” International Journal of Innovative Research in Science, Engineering and Technology, Vol. 6(6), pp. 10690-10695, 2017
[8] Janwal, P., Mittal, A. K. and Mouchel, J. “Efficiency evaluation of sewage treatment plants with different technologies in Delhi (India)”, Environmental Monitoring and Assessment, Vol. 153(1-4), pp. 293-305, 2009
[9] Kotz, S. and Johnson, N. “Process Capability Indices, Ist ed.”, Chapman and Hall, London, 1993.
[10] Kotz, S. and Lovelace, C. “Process Capability Indices in Theory and Practice, Ist ed.\textdagger”, Arnold, London, 1998
[11] Corbett, Charles & Pan, Jeh-Nan. “Evaluating environmental performance using statistical process control techniques” European Journal of Operational Research. Vol. 139(1), pp. 68-83, 2002

**Fig. 2. Histogram of estimator of MCP_u(p)**

Interpretation: Here wastewater treatment plant is not capable to meet the effluent discharged standards for wastewater treatment plant developed by CPCB because estimated values of MPCI; $MCP_u(p)$ is too less as compare to desirable value 1. This is also reflected through 95% confidence interval of $MCP_u(p)$. In view of univariate process capability, process is not capable with respect to all variables. This statement is based on values of $CP_u(p)$ for each variable.

To improve process capability we need to improve process capability with respect to all variables. Root cause analysis is needed to identify root causes of low capability with respect to all variables.
[12] Jeh-Nan Pan, Chung-I Li and Wei-Chen Shih “New multivariate process capability indices for measuring the performance of multivariate processes subject to non-normal distributions”, International Journal of Quality & Reliability Management, Vol. 33(1), pp. 42-61, 2016

[13] Shinde, R.L. and Khadse, K.G. “A review and comparison of some multivariate process capability indices based on fraction conforming interpretation”, Statistical Methods, Vol. 7(2), pp. 95-115, 2005

[14] Khadse, K.G. and Shinde, R.L. “Probability based Process Capability Indices”, Communications in Statistics - Simulation and Computation; Vol. 38(4), pp. 884-904, 2009

[15] Shinde, R.L. and Khadse, K.G. “Multivariate Process Capability using Principal Component Analysis”, Quality Reliability Engineering International, Vol. 25(1), pp. 69–77, 2009

[16] de-Felipe, D. and Benedito, E. “A Review of univariate and multivariate process capability indices”, Int J Adv Manuf Technol, Vol. 92(5-8), pp. 1687-1705, 2017

[17] Bhave, P.P., Naik, S. & Salunkhe, S.D. “Performance Evaluation of Wastewater Treatment Plant”, Water Conservation Science and Engineering 2020, in press.