OGLE-2014-BLG-0962 and the First Statistical Validation of Bayesian Priors for Galactic Microlensing

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ABSTRACT

OGLE-2014-BLG-0962 (OB140962) is a stellar binary microlensing event that was well-covered by observations from the Spitzer satellite as well as ground-based surveys. Modelling yields a unique physical solution: a mid-M+M-dwarf binary with $M_{\text{prim}} = 0.20 \pm 0.01 M_\odot$ and $M_{\text{sec}} = 0.16 \pm 0.01 M_\odot$, with projected separation of 2.0 ± 0.3 AU. The lens is only $D_{\text{LS}} = 0.41 \pm 0.06$ kpc in front of the

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source, making OB140962 a bulge lens and the most distant Spitzer binary lens to date. In contrast, because the Einstein radius ($\theta_E = 0.143 \pm 0.007$ mas) is unusually small, a standard Bayesian analysis, conducted in the absence of parallax information, would predict a brown dwarf binary. We test the accuracy of Bayesian analysis over a set of Spitzer lenses, finding overall good agreement throughout the sample. We also illustrate the methodology for probing the Galactic distribution of planets by comparing the cumulative distance distribution of the Spitzer 2-body lenses to that of the Spitzer single lenses.

**Keywords:** gravitational lensing: micro – binaries: general – stars: low-mass – Galaxy: bulge – methods: statistical

1. INTRODUCTION

Gravitational microlensing is a type of transient phenomenon in which a temporary alignment of a foreground lens and a background source causes the source to be magnified. Because lensing is sensitive to the presence of mass independent of any associated flux, it represents a unique means to probe distant and faint populations of many compact astrophysical objects of interest (e.g. low-mass main-sequence stars, brown dwarfs, planets, and stellar remnants). Indeed, microlensing has discovered stellar remnants (e.g. Shvartzvald et al. 2015; Wyrzykowski et al. 2016) and free floating planets (e.g. Sumi et al. 2011; Mróz et al. 2017, 2018), as well as characterized planets and low-mass objects anywhere between the Sun and the Galactic center.

One drawback of the microlensing technique is that, while relative parameters such as mass ratios (for binaries) are routinely measured, it is often difficult to infer the absolute physical properties of the lens from a ground-based light curve alone. For many applications, the absolute physical properties of the lens – its mass ($M_L$), distance ($D_L$), and lens-source relative kinematics ($\vec{v}_{\text{rel}}$) – are paramount to interpretation. For example, in characterizing individual lensing systems, incertitude in the physical parameters can make the difference between a star, a brown dwarf, a planet, or a moon (e.g. Bennett et al. 2014; Albrow et al. 2018). To study the distribution of planet masses from an ensemble of binary lens mass-ratios (Shvartzvald et al. 2016a; Suzuki et al. 2016), the host masses are needed. Measurement of planetary occurrence rate as a function of distance and Galactic environment (e.g. Penny et al. 2016) also depends on whether the system distances and kinematic memberships are reliably assigned on average.

The challenge of determining physical quantities for lenses from ground-based data alone arises because 4 parameters are needed to constrain the 4 physical properties (that is, 2 scalar quantities: $M_L$ and $D_L$, and 1 vector quantity with 2 components: $\vec{v}_{\text{rel}} = [v_{\text{rel},N}, v_{\text{rel},E}]$). The microlensing parameters $t_E$ (Einstein timescale), $\theta_E$ (Einstein radius), and $\pi_E$ (microlensing parallax) form a complete set that can be solved for the physical parameters (see Section 3.1). However, only $t_E$ is readily measured for microlensing events. One can measure $\theta_E$ using the finite-source effect, which is not usually present for single-lens events but often feasible for binary lensing. This leaves $\pi_E$ which, prior to Spitzer, was not accessible for most events because their $t_E$ is considerably less than 1 year.

In most cases for which $\pi_E$ is not available, a Bayesian analysis can be used to obtain a posterior on the physical properties of a particular event. This is done by forward modelling individual source and lens stars in the Galaxy to match with the measured $t_E$ and $\theta_E$ of the event. The priors for such a model integrate kinematics, stellar density profiles, and mass functions for the Galactic disk and bulge. Since most microlensing events will have ground-based survey data only, Bayesian analysis will continue to be the leading avenue used to estimate the physical parameters of microlensing systems, until the WFIRST (Spergel et al. 2013) era.

Given the importance of physical parameters for the correct interpretation of lensing systems, it is critical to examine the accuracy of Bayesian analysis – that is, to compare its predictions to the ‘true’ values determined from other means. One way to arrive at the ‘true’ answers is to perform followup adaptive optics (AO) imaging, specifically to resolve the source and lens separately. Notably, AO solutions were obtained in a handful of cases, finding generally good agreement with the original Bayesian predictions. For example, Batista et al. (2014) found the host mass and distance of MOA-2011-BLG-293 to be $M_L = 0.86 \pm 0.06 M_\odot$ and $D_L = 7.72 \pm 0.44$ kpc, fully consistent with the Bayesian predictions of $M_L = 0.59_{-0.29}^{+0.35} M_\odot$ and $D_L = 7.15 \pm 0.75$ kpc (Yee et al. 2014).
et al. 2012). For OGLE-2005-BLG-169, Bennett et al. (2015) and Batista et al. (2015) retrieve physical properties ($M_L = 0.69 \pm 0.02 M_\odot$ and $D_L = 4.1 \pm 0.4$ kpc) consistent with the original Bayesian result from Gould et al. (2006) ($M_L = 0.49^{+0.23}_{-0.29} M_\odot$ and $D_L = 2.7^{+1.5}_{-1.3}$ kpc).

Simultaneous observation by a distant satellite provides another way to obtain the "true" parameters of a microlensing event. Since microlensing events involve very precise alignment between the lens system and the source star trajectory, the alignment angle is different for two widely separated observers, leading to inter-light source star trajectory, the alignment angle is different. Since microlensing events involve

This principle motivated the Spitzer microlensing campaign which, since its inaugural year in 2014, has yielded numerous parallax measurements to single lenses (e.g. Calchi Novati et al. 2015a; Yee et al. 2015a; Zhu et al. 2017). Moreover, Spitzer has helped to measure $\theta_E$ and $\pi_E$ for a dozen stellar binaries (e.g. Bozza et al. 2016; Han et al. 2017; Wang et al. 2017) and planets (e.g. Udalski et al. 2015b; Street et al. 2016; Shvartzvald et al. 2017; Ryu et al. 2018), disentangling the absolute physical properties of the lens systems.

The Spitzer sample also forms an ideal test bed for Bayesian analysis. At least two Spitzer objects have published Bayesian analysis results. The physical properties of the single-lens OB151482 found by detailed modelling of the finite source effect (Chung et al. 2017) yielded a mass and distance consistent with a Bayesian analysis presented by Zhu et al. (2017) for the same object. However, for the low mass-ratio planet OB161195, Bond et al. (2017)'s Bayesian predictions are in tension with the parameters found by a full modelling including the Spitzer light curve presented in Shvartzvald et al. (2017).

The variation in the results for AO and parallax tests indicate the need for a systematic test of the Bayesian method as compared to traditional measurements. This work presents the discovery of OGLE-2014-BLG-0962 (OB140962), a textbook example of a stellar binary lens with excellent data coverage from both the ground and Spitzer, leading to superbly constrained physical parameters. We describe the data in Section 2 and the modelling process in Section 3. In particular, we include the mathematical relations between the microlensing and physical parameters of interest in Section 3.1. The unique physical properties for this lens are given in Section 4, where we find that this binary is likely the most distant stellar binary detected by Spitzer to date, almost certainly a member of the Galactic bulge.

In Section 5 we start by performing Bayesian analysis on OB140962 while withholding the parallax information (Section 5.2). We subsequently repeat this analysis for Spitzer events with secure parallax-derived physical parameters to investigate the overall reliability of Bayesian analysis.

Finally, in Section 6, we compare the distribution of well-characterized Spitzer binaries (including planets) to that of the Spitzer single lenses. This serves to illustrate how one might quantify the relative occurrence rate of planets and binaries throughout the Galaxy when a larger sample becomes available and selection effects are systematically quantified. Section 7 provides a summary.

2. OBSERVATIONS

OGLE-2014-BLG-0962 (hereafter OB140962) was located at equatorial coordinates $(\alpha, \delta)_{2000} = (18:01:42.98, -27:55:56.2)$. These translate into Galactic coordinates $(l, b) = (2.7^\circ, -2.5^\circ)$. It was alerted by the Optical Gravitational Lensing Experiment Early Warning System (OGLE: Udalski et al. 2015a; EWS: (Udalski 2003)) at UT 18:53, 30 May 2014, in time to mobilize immediate followup observations by the first Spitzer microlensing campaign (e.g. Udalski et al. 2015b; Yee et al. 2015b). The light curve, as shown in Figure 1, is a caustic crossing event that reveals a clear signature of a high mass-ratio binary lens. The caustic entrance and exit are well covered by both ground- and space-based (§2.2) observations, leading to secure determination of microlensing and physical lens parameters. Prior to modelling, the errors on the photometric reduction from each observatory were rescaled according to standard procedures and clipped for outliers (§2.3).

2.1. Ground-based Observations

The OGLE observations are conducted with the 1.3m Warsaw telescope at the Las Campanas Observatory in Chile, with a 1.4 deg^2 field of view (FoV) camera. Data in the $I$-band were taken at a nominal cadence of $\Gamma = 1$ hr$^{-1}$. The regions around and between the caustic crossings are well-sampled. $V$-band data were also acquired at a lower cadence. Four points, including one near peak, were captured in OGLE $V$-band between HJD = 6810 and 6830. OGLE photometry was reduced with the Difference-Imaging Analysis (DIA) method (Alard & Lupton 1998; Wozniak 2000). The Microlensing Observations in Astrophysics (MOA) collaboration also observed this event (MOA-2014-BLG-285). MOA provided an alert on 31 May 2014. The MOA survey is conducted from the University of Canterbury Mt John Observatory in New Zealand, which features a 1.8 m telescope with a camera whose FoV...
Figure 1. The ground- and space-based light curves of binary microlensing event OGLE-2014-BLG-0962, including data from OGLE, MOA, Wise, and Spitzer. The best-fit $u_0 > 0$ model is shown in black, while the purple curve outlines the corresponding space-based solution. The inset shows a zoom-in of the highly magnified portion.

is 2.2 deg$^2$. MOA observes in the custom $R_{\text{MOA}}$-band, which is approximately the superposition of the standard $I$ and $R$-bands. Normally MOA surveys at high cadence, though for this particular event it missed the portion of the light curve between the caustic entrance and exit due to weather. MOA photometry is reduced by the DIA pipeline summarized in Bond et al. (2001).

The Wise microlensing survey (Shvartzvald et al. 2016a) used the 1 m telescope at Tel Aviv University’s Wise Observatory in Israel. The Large Area Imager for the Wise Observatory camera with (FoV = 1 deg$^2$) was used to collect data on this event in survey mode. Wise observations are conducted in the $I$-filter. The nominal cadence is 30 min, averaging $\sim$ 5 to 6 observations per night due to target visibility. Photometry for Wise is performed with the DIA software described in Albrow et al. (2009).

2.2. Space-based Observations

OB140962 was observed in the first season of the Spitzer microlensing campaign, before the development of the objective target selection procedure of Yee et al. (2015b), which was used in subsequent seasons. Spitzer observations were taken in the $L$-band (3.6μm). The
target was selected for Spitzer observations before it showed any features attributable to a binary. Observations began on 6 June 2014 (HJD’ = 6814.59). The last data point was taken on 10 July 2014 (HJD’ = 6849.34). A total of 31 observations were taken at a cadence of $\Gamma \sim 1$ day$^{-1}$. It captured several points during the anomaly. Spitzer photometry was reduced with the pipeline presented in Calchi Novati et al. (2015b).

2.3. Error Rescaling

Purely photometric (i.e., Poisson) errors are often underestimated, which prompts a rescaling of the data points and renormalization of the errors. Except for the OGLE errors, which are rescaled based on the recommended procedure of Skowron et al. (2016), errors from the other observatories (in magnitudes) are modified using the scheme of Yee et al. (2012)$^1$, where:

$$
\sigma_{\text{rescaled}} = k \sigma_{\text{pipeline}}. \tag{1}
$$

With $\sigma_{\text{rescaled}}$, every data point should contribute $\sim 1$ in $\chi^2$ on average. The $k$-factor is adjusted manually until this is the case. The newly scaled errors are used to reject outliers and updated iteratively. As a result, we reject four OGLE, two MOA, and two Wise measurements. The final adopted $k$ parameters are listed in Table 1.

### Table 1. Error Rescaling Factors for Each Observatory

| Observatory | $k$          |
|-------------|-------------|
| OGLE        | See Skowron et al. (2016) |
| MOA         | 1.25        |
| Wise        | 1.46        |
| Spitzer     | 7.9         |

| Observatory | $k$          |
|-------------|-------------|
| OGLE        | See Skowron et al. (2016) |
| MOA         | 1.25        |
| Wise        | 1.46        |
| Spitzer     | 7.9         |

3. ANALYSIS

In this section we deduce the microlensing parameters and physical lens properties via joint modelling of the ground- and space-based light curves. In §3.1 we introduce the relevant parameters that can be measured from our data and describe how to use them to obtain the absolute physical properties. But even prior to rigorous modelling, many conclusions can be drawn from the data points alone thanks to the comprehensive coverage of the event from both the ground and space. Therefore, in §3.2 we provide a heuristic description of the light curve, which yields basic insight into the nature of the microlensing event. §3.3 summarizes the multi-staged modelling process to eventually arrive at the microlensing parameters.

3.1. Microlensing Parameters & Relations to Physical Properties

There are six fundamental parameters associated with and routinely measured for binary lensing light curves: $(t_0, u_0, t_s, s, q, \alpha)$. The first three quantities stand for the peak time, impact parameter of the source trajectory to the lens (scaled to the lens Einstein radius, $\theta_E$, see below), and the Einstein time scale, i.e., the characteristic width of the portion of the light curve undergoing magnification. The second set of 3 parameters pertain to the binary lens. They are: the instantaneous projected separation between the components (normalized to $\theta_E$), their mass ratio, and the projected angle of the source trajectory to the binary axis, respectively.

All the parameters presented so far are either geometric or relative. Of course, it is the absolute physical properties of the lens that are of greatest interest. The lens mass ($M_L$), distance ($D_L$), and relative proper motion between the lens and source ($\mu_{\text{rel}}$) can be determined provided additional effects are measured. They are linked to the direct observables via the Einstein radius ($\theta_E$) and the dimensionless vector microlensing parallax ($\hat{\pi}_E$). For $\pi_{\text{rel}} \equiv \pi_L - \pi_S = \text{AU}(D_L^{-1} - D_S^{-1})$, $D_S$ being the source distance (usually close to the Galactic center at $\sim 8.3$ kpc), $\theta_E$ and $\hat{\pi}_E$ are defined as follows (e.g. Gould 2000):

$$
\theta_E \equiv \sqrt{\kappa M_L \pi_{\text{rel}}}; \quad \kappa \equiv \frac{4G}{c^2 \text{AU}} \approx 8.14 \text{mas} \frac{\text{AU}}{M_\odot}; \quad (2)
$$

and

$$
\hat{\pi}_E \equiv \pi_{\text{rel}} \frac{\hat{\mu}_{\text{rel}}}{|\theta_{\text{rel}}|}; \quad \mu_{\text{rel}} = \frac{\theta_E}{t_E}. \tag{3}
$$

Manipulating Equations (2) and (3), both the lens mass and distance can be expressed as a function of $\theta_E$ and $\pi_E$:

$$
M_L = \frac{\theta_E}{\kappa \pi_E}; \quad D_L = \frac{\text{AU}}{\pi_E \theta_E + \text{AU}/D_S}. \quad (4)
$$

For caustic-crossing events, the finite source effect constrains a 7th parameter $\rho$, where

$$
\rho \equiv \frac{\theta_s}{\theta_E} = \frac{t_s}{t_E}, \tag{5}
$$

i.e. the size of the source $\theta_s$ measured in units of $\theta_E$. If the source radius can be deduced independently, for
instance from the event’s position in the local color-magnitude diagram (CMD), then \( \theta_E \) can be calculated. Alternatively, \( \rho \) can be defined as the source self-crossing time, \( t_\star \), relative to \( t_E \).

The microlensing parallax, \( \pi_E \), can be measured with a second line of sight to the event, which generally will result in a light curve with timing and morphology that are distinct from the first because of the apparent difference in trajectory. A useful qualitative approximation for the components of \( \pi_E \) is given by the scaled difference in the \( t_0 \) and \( u_0 \) between the two sight lines (e.g. Refsdal 1966):

\[
\pi_E = \frac{\text{AU}}{D_\perp} \begin{pmatrix} \Delta t_0 ; \Delta u_0 \end{pmatrix}
\]

(6)

where \( D_\perp \) is the projected separation vector between the two observing locations in the plane of the sky. Equation (6) applies for the coordinate system in which the x-axis is aligned with \( D_\perp \). For Earth and the Spitzer satellite, the magnitude of this vector is approximately 1 to 1.5 AU. Refer to, e.g., Equations (8) to (10) in Calchi Novati et al. (2015a) for the exact relation between \( \pi_E \), \( \Delta t_0 \), \( \Delta u_0 \), and instantaneous \( D_\perp \), which is used in the actual modelling for \( \pi_E \).

3.2. Heuristic Description of the Light Curve

The ground-based light curve has a broad double-horned structure characteristic of roughly equal mass-ratio binary lensing, exhibiting a clear caustic entrance (HJD’ = HJD-2450000 \( \sim \) 6816.6) and exit (HJD’ \( \sim \) 6818.3). The hump in the light curve immediately following the caustic exit (HJD’ \( \sim \) 6819.0) implies a cusp approach. The shape and timing of these features place tight constraints on the event geometry. Below we illustrate the back-of-the-envelope process of converting the lightcurve components into microlensing parameters and interpret the inferred physical properties of the source-lens system.

We approximate this event to have zero blending and estimate the Einstein timescale \( (t_E) \) from the half-width of the magnified portion of the light curve at 1.3 \( \times \) the baseline flux. For this event, \( t_E \sim 5 \) days. The caustic crossings resolve the source size (i.e., finite source effect), allowing us to determine \( \theta_E \) from Equation (5). Figure 1 shows the half-width of the caustic entrance is \( t_\star \sim 0.15 \) days, thus \( \rho \approx 0.03 \). To obtain \( \theta_\star \), we note that the event placement in the local color-magnitude diagram is consistent with a bulge giant (Figure 2 and Section 4.1). A typical clump giant might have radius 5 to 10\( \times \) that of the Sun, say \( \theta_\star \approx 4 \mu \text{as} \). Then, \( \theta_E \approx 0.13 \text{mas} \).

Together with \( t_E \) and Equation (3), we find that the relative lens-source proper motion is \( \mu_{\text{rel}} \approx 9.5 \text{mas/yr} \).

Figure 2. The local color-magnitude diagram around OB140962. The red giant clump centroid is located at the center of the red circle.

For many microlensing discoveries with only ground-based data, deducing \( \theta_E \) and \( \mu_{\text{rel}} \) is as far as we can go. To estimate the absolute physical properties of the lens, we might assume the lens has a typical distance of \( D_L \sim 6 \) kpc. Assuming a source distance of \( D_S \sim 8.3 \) kpc, \( \pi_{\text{rel}} \approx 0.046 \). Then, substituting \( \theta_E \approx 0.13 \) mas into Equation (2) gives \( M_{\text{tot}} \approx 0.045 M_\odot \). Therefore, the atypically small \( \theta_E \) for this event (normally \( \sim 0.5 \) mas) implies an exciting low-mass BD-BD binary.

For this event we have parallax information, which constrains the true lens distance and mass. To estimate \( \pi_E \), we see from Equation (6) that \( |\pi_E| \approx \sqrt{(\Delta t_0/t_E)^2 + (\Delta u_0)^2} \), where we have used the fact that \( D_\perp \) is of order 1 AU. For OB140962, the Spitzer light curve actually closely mimics the ground-based one in shape as well as timing — offset by \( \Delta t_0 \sim 0.3 \) days. The virtually indistinguishable light curve morphologies between the two sightlines strongly implies nearly identical impact parameters between the two events (i.e., \( \Delta u_0 \) negligible), so \( \pi_E \sim \Delta t_0/t_E \approx 0.06 \). The physical
parameters $M_{\text{tot}}$ and $D_L$ can both be computed from $\theta_E$ and $\pi_E$. According to Equation (4), $M_{\text{tot}} \approx 0.27M_\odot$ and $D_L \approx 7.8$ kpc. Here we have assumed that the source is located at the Galactocentric distance $R_0 \approx 8.3$ kpc. Therefore, from this heuristic evaluation of the ground light curves in conjunction with the Spitzer parallax, we reach the conclusion that the lens is a typical low-mass binary that must be very close to the source. This is at odds with the earlier expectation of a very low-mass lens from $\theta_E$ and $\mu_{\text{rel}}$ alone.

### 3.3. Modelling the Light Curve

To map the overall topology of the parameter space for the ground-based light curve, we perform a grid search in $\chi^2$-space over $\log s$, $\log q$, and $\alpha$, which are responsible for the magnification profile of the event (Dong et al. 2006). For each point (log $s \in [-1,1]$, log $q \in [-5,1]$, $\alpha \in [0,2\pi]$) on the $100 \times 100 \times 21$ grid, we allow the other light curve parameters ($u_0$, $\theta_E$, $E$, $\rho$) to be explored by a Markov Chain Monte Carlo (MCMC) until it settles on the minimal $\chi^2$. We find the global minimum $\chi^2$ to be in the region around log $s \sim 0.3$ and log $q \sim 0.07$ (based on modelling the OGLE $I$-band data prior to error rescaling).

From the best-fit grid point we launch our full MCMC for a joint fit for all four data sets (3 ground, 1 space). The finite source effect is modelled using the ray-shooting method (Schneider & Weiss 1986; Kayser et al. 1986; Wambsganss 1997) and regions of the light curve immediately adjacent to caustic crossings are computed through the hexadecapole approximation (Gould 2008; Pejcha & Heyrovský 2009). With the inclusion of the space data, two additional parameters associated with the space parallax are fit: $\pi_{E,i} = (\pi_{E,N}, \pi_{E,E})$. We modelled the limb-darkening of the source star using the parameters derived in §4.1. The final best-fit solutions are compiled in Table 2. The parameter errors presented are 16% and 84% confidence intervals (CIs), evaluated from the MCMC posteriors.

Single-lens satellite parallax suffers from the well-known 4-fold degeneracy (e.g. Refsdal 1966; Gould 1994). For binary lensing, depending on the data quality and coverage, some degeneracies can be resolved (see discussion in, e.g., Zhu et al. 2015). OB140962 has a well-covered light curve from both the ground and space, leading to a straightforward interpretation. In this case, the $u_0 > 0$ and $u_0 < 0$ degeneracy persists, but maps into nearly identical physical properties. Therefore, the physical solution is unique. In Figure 1 we plot the $u_0 > 0$ solution based on the corresponding best-fitting parameters. Figure 3 shows the associated caustic structure.

A comparison between the final fitted microlensing parameters and those from the heuristic assessment of §3.2 reveals that they are qualitatively consistent.

We also fit for higher order effects in the OGLE $I$-band light curve but we found that no meaningful constraints could be placed on the annual parallax and orbital motion from these data alone. This is unsurprising because these phenomena typically manifest on timescales of tens to hundreds of days. In contrast, OB140962 is magnified for merely $\sim 10$ days, with only $\sim 2$ days between caustic crossings.

### 4. PROPERTIES OF THE SOURCE AND LENS

#### 4.1. Source Star Limb Darkening and Angular Radius

The source star properties can be inferred from its position on the local CMD. We calculate the apparent source $(V-I)$ color by fitting a line to the observed event flux in the OGLE $V$ vs. OGLE $I$-band. This yields a model-independent color of $(V - I) = 1.963 \pm 0.006$. 

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Figure 3. The $u_0 > 0$ caustic structure of the binary microlensing event OB140962. This is a resonant caustic crossing event. The source size is indicated by the orange circle. Lower panels show zoom-ins of the ground (black)- and space (purple)-based source trajectories, with miniscule separation between them. Arrow tips coincide with $t_0$ for the ground-based light curve.
Modelling the source flux yields an apparent $I$-band magnitude of 16.22 ± 0.01.

Using the observed $(V - I)$ vs. $I$ CMD from OGLE in the field of the target, we locate the red clump. The apparent clump centroid is $(V - I, I)_{\text{clump}} = (2.215, 15.59)$. According to Bensby et al. (2013) and Nataf et al. (2013), the intrinsic color and magnitude of the red clump in the event direction is $(1.06, 14.36)$. Using the offset between the observed and actual clump centroid as a measure of source extinction and reddening (Yoo et al. 2004), we determine the intrinsic source color and brightness to $(V - I, I)_{\text{source}} = (0.808, 14.98)$. From Bessell & Brett (1988)'s color table for giants, we infer the source to be a G0 giant.

We interpolate the color tables in Bessell & Brett (1988) to arrive at a $(V - K, K)_{\text{source}} = (1.78 \pm 0.04, 14.00 \pm 0.06)$. Using the relationship between stellar angular size, $(V - K)$ color, and $K$-magnitude given by Adams et al. (2018), the source angular radius $\theta_* = 3.4 \pm 0.2$ mas.

The source star's brightness profile, which is important for modelling the caustic crossings, is parametrized by its limb darkening properties. Claret & Bloemen (2011) gives linear limb darkening coefficients $(u)$ for stars with a variety of effective temperatures, surface gravities, metallicities, and microturbulences. Assuming solar metallicity, we determine $T_{\text{eff}}$ to be 5400 ± 100K using its relation with $V - I$ color from Casagrande et al. (2010). We adopt log($g$) = 3 and microturbulence ~ 2 km/s. The corresponding $\Gamma = (2u/(3 - u))$ is 0.41 in the $I$-band and 0.14 in Spitzer $L$-band. These $\Gamma$ values are in turn used in the final fits of the light curve parameters as described in §3.3.

4.2. Physical Parameters of the Lens

From the equations listed in §3.1, the physical properties of the system are straightforwardly determined. We display the results in Table 3. The uncertainties are derived from direct propagation. We calculate $D_L$, $a_{\text{proj}}$, and $D_{LS}$, assuming zero uncertainty in $D_S$. These final calculated properties are broadly compatible with the estimates from the earlier heuristic arguments.

| Quantity         | Value from Best-Fit Solution |
|------------------|------------------------------|
|                  | $u_0 > 0$                    | $u_0 < 0$                    |
| $\pi_E$          | 0.049±0.001                 | 0.048±0.001                 |
| $\theta_E$ (mas) | 0.144±0.008                 | 0.144±0.008                 |
| $\mu_{\text{rel}}$ (mas/yr) | 8.119±0.001 | 8.132±0.001 |
| $M_{\text{tot}}(M_\odot)$ | 0.365±0.020 | 0.366±0.020 |
| $M_{\text{prim}}(M_\odot)$ | 0.204±0.011 | 0.205±0.011 |
| $M_{\text{sec}}(M_\odot)$ | 0.160±0.009 | 0.161±0.009 |
| $D_S$ (kpc)       | 7.863±0.000                 | 7.836±0.000                 |
| $D_L$ (kpc)       | 7.453±0.021                 | 7.455±0.021                 |
| $a_{\text{proj}}$ (AU) | 2.04±0.107 | 2.03±0.107 |
| $D_{8.3}$ (kpc)   | 7.845±0.021                 | 7.847±0.021                 |
| $D_{LS}$          | 0.410±0.021                 | 0.407±0.021                 |

Since the exact source distance is unknown, we list both $D_{8.3}$ (Calchi Novati et al. 2015a) and $D_L$, which is relative to the mean bar clump distance at the event’s Galactic coordinates, which is $D_S = 7.86$ kpc (Nataf et al. 2013). Regardless of the precise location of the source, this M+M-dwarf binary is the farthest lensing systems discovered with Spitzer.

5. THE SPITZER MICROLENS SAMPLE: A TESTBED FOR BAYESIAN ANALYSIS
OB140962 represents another addition to the growing sample of well-characterized microlensing systems from the Spitzer satellite parallax campaign. This set of objects have directly measured $M_L$ and $D_L$, in contrast to most microlensing discoveries to date, whose physical properties are indeterminate due to the lack of constraint on $\pi_E$. For the caustic-crossing microlensing events for which $t_E$ and $\theta_E$ are typically measured, the standard way to proceed is to perform a Bayesian analysis to infer probabilistic distributions for these parameters. This involves evaluating the likelihood of particular lens-source configurations using a Galactic model prior conditioned upon the measured $t_E$ and $\theta_E$ (taken together, they also encode the magnitude of the lens-source relative proper motion, see Equation (3)). The resulting posteriors are often broad, with CIs spanning about a half-dex in mass and 2-3 kpc in distance. In Section 5.1, we describe the ingredients that go into such an analysis.

It is important to have confidence in the conclusions from the Bayesian analysis, since this will remain the chief channel for deriving lens system properties in the absence of expensive simultaneous satellite observations. They will continue to affect our understanding of both individual systems and ensemble statistics (e.g. Calchi Novati et al. 2015a; Penny et al. 2016).

The Spitzer sample provides an excellent opportunity to test the accuracy of Bayesian analysis for ~ a dozen systems (Table 4). In Section 5.2, we demonstrate such a comparison for OB140962. Then, in Section 5.3, we extend this test to the subset of Spitzer microlenses published to date with similarly secure characterizations.

### 5.1. Bayesian Formalism

The Bayesian analysis framework is based on a Galactic model prior, whose ingredients are velocity distributions (VD), mass functions (MF), and density profiles (DP) of the bulge and disk of the Milky Way, in the direction of the event. Each draw of a lens-source pair has a corresponding $\theta_E$ and $\mu_{rel}$ (which is interchangeable with $t_E$). For binary lenses, we make the following modification to the original Bayesian formalism, whose mass function assumes single stars and does not account for binaries. We draw the mass of the primary component, $M_{\text{prim}}$, assuming that it follows the single-star MF from Chabrier (2003). Then we calculate $M_{\text{tot}}$ and $\theta_E$ from $M_{\text{tot}} = M_{\text{prim}}(1 + q)$. One underlying assumption is that the binary parameters of the event $(s, q)$ do not depend on the mass and distance of the lens. The likelihood function is constrained by the observed $t_E$ and $\theta_E$ of the event. For a detailed description of the Galactic model used in this work, see Jung et al. (2018), which draws from Han & Gould (1995, 2003), and Batista et al. (2011). Alternative models, varying some or all of the three components described above, are also used in literature (e.g. Bennett et al. 2014; Zhu et al. 2017).

#### 5.2. OB140962

We input our best-fit $\theta_E$ and $t_E$ values from the $u_0 > 0$ solution into the Bayesian analysis. Figure 4 displays the posterior distributions for $M_{\text{prim}}$ and $D_{\text{LS}}$. $D_{\text{LS}}$ is a more robust metric than $D_L$, since it is largely independent of the uncertainty in the source distance. The directly measured quantities are over-plotted. Bayesian analysis indicates that the lens’ primary has $\log(M_{\text{prim}} / M_\odot) = -1.15^{+0.43}_{-0.35}$ or $M_{\text{prim}} = 0.07^{+0.12}_{-0.039} M_\odot$. The true value of $M_{\text{prim}} \sim 0.20$ is just outside the 68% CI. In this case, the difference between the Bayesian value and the true value means the difference between a brown-dwarf binary detection and a run-of-the-mill M+M binary. Similarly, the parallax-derived value of 0.41 kpc is outside the 68% CI of the Bayesian prediction for the lens-source distance $D_{\text{LS}} = 1.38^{+1.22}_{-0.77}$ kpc. The very small $\pi_E$ measured by Spitzer places the true lens very close to the source star. It is clear that Spitzer has provided important added value for accurately determining the mass and distance to this microlens.

#### 5.3. Other Spitzer Microlensing Systems

Bayesian analysis is expected to give a statistical representation of the truth. As such, it is not in itself surprising that individual outliers like OB140962 exist. The growing inventory of objects with Spitzer satellite parallaxes allows us to investigate whether there are systematic problems with the Bayesian framework for a larger sample.

We repeat the Bayesian analysis for the 13 published Spitzer events (including OB140962) with unique measurements of both $\pi_E$ and $\theta_E$. Their relevant properties are given in Table 4. Among their ranks are both two-body lenses and single lenses with securely modelled finite-source effects. We treat binaries as described in §5.1. For planetary events (defined for this purpose to be $q < 0.05$), we exclude stellar remnants from the Galactic models. For events with degeneracies for which the authors advocate strongly for one particular solution for $\theta_E$ and $\pi_E$ based either on $\chi^2$ fitness or on physical grounds (OB140289: Udalski et al. 2018; OB141050: Zhu et al. 2015; OB161045: Shin et al. 2018; OB161190: Ryu et al. 2018), we retain the favoured solutions only. Events with degeneracies yielding physical properties consistent
The result is summarized in Figure 5. For the majority of the cases, the Bayesian posteriors are consistent with the true measured values. One of the outliers in the Bayesian prediction compared to the result derived from parallax belongs to OB140962 (see Section 5.2), for which the true value lies above the 84th percentile of its Bayesian posterior. However, if the posteriors are true representations of the data, occasional outliers are expected. In fact, this particular situation should occur for 16% of the instances.

We exclude from our Bayesian sample the events with severe degeneracies, i.e. those with multiple solutions for which the physical properties \( M_L \) and \( D_L \) are incompatible within their nominal uncertainties (OB150196: Han et al. 2016; OB150479: Han et al. 2016; OB151195: Shvartzvald et al. 2017). Note that, although membership in our sample requires selection due to the absence of the finite source effect, membership in our sample requires selection based on the solution with the lowest \( \chi^2 \) for this comparison (OB140124: Udalski et al. 2015b; Beaulieu et al. 2018; OB141050: Zhu et al. 2015; OB150479: Han et al. 2016; OB161045: Shvartzvald et al. 2016b). Therefore, we assign to it physical parameters determined by followup AO (Beaulieu et al. 2018). In the case of OB140289, Spitzer could not constrain \( \pi_E \) because it happened to observe a featureless region of the light curve. Fortuitously, this event is sufficiently long such that annual parallax could be accurately and precisely determined.

Within 1σ are assigned physical properties corresponding to the solution with the lowest \( \chi^2 \) for this comparison (OB140124: Udalski et al. 2015b; Beaulieu et al. 2018; OB141050: Zhu et al. 2015; OB150479: Han et al. 2016; OB161045: Shvartzvald et al. 2016b). Note that, although membership in our sample requires selection due to the absence of the finite source effect, membership in our sample requires selection based on the solution with the lowest \( \chi^2 \) for this comparison (OB140124: Udalski et al. 2015b; Beaulieu et al. 2018). In the case of OB140289, Spitzer could not constrain \( \pi_E \) because it happened to observe a featureless region of the light curve. Fortuitously, this event is sufficiently long such that annual parallax could be accurately and precisely determined.

We exclude from our Bayesian sample the events with severe degeneracies, i.e. those with multiple solutions for which the physical properties \( M_L \) and \( D_L \) are incompatible within their nominal uncertainties (OB150196: Han et al. 2016; OB151482: Chung et al. 2017; OB170329: Han et al. 2018). It would be difficult to interpret a comparison between the Bayesian results and quantities that are ill-defined. We also exclude OB151285 (Shvartzvald et al. 2015) and OB161266 (Albrow et al. 2018) from this exercise since the Bayesian priors for the mass function of planetary-mass objects and stellar remnants are not well understood. The literature does not homogeneously report the source distance assumed in the \( D_L \) calculations. Therefore, for consistency, we calculate \( D_{LS} \) for each system using the clump distance in the direction of the event (Nataf et al. 2013) as \( D_S \).

In the case of OB140289, Spitzer could not constrain \( \pi_E \) because it happened to observe a featureless region of the light curve. Fortuitously, this event is sufficiently long such that annual parallax could be accurately and precisely determined.
Figure 4. Posteriors of lens physical properties ($M_{\text{prim}}$ and $D_{\text{LS}}$) for OB140962 based on Bayesian analysis. The Bayesian median is demarcated by the black dashed verticals, while the yellow shaded boxes outline the 68% CIs about the median. Overplotted in the magenta dash-dotted lines are the values measured directly from Spitzer parallax. Whereas the Bayesian analysis argues for a brown dwarf binary, the Spitzer measurement clearly attributes the event to a mid-M+M-dwarf binary lens very close to the Galactic center. Only $\sim 14\%$ ($\sim 9\%$) of the Bayesian posterior lies above (below) the true $M_L$ ($D_{\text{LS}}$).

should expect this CDF to follow the identity function (e.g. 10% of the time the true value falls below 10% of the posterior). In Figure 6 we show the cumulative distribution of the fraction of posterior lying above the parallax value for $M_L$ and $D_{\text{LS}}$. One-sample Kolmogrov-Smirnov (KS) tests show that neither parameters are significantly differently distributed from the 1-to-1 line. This indicates that, on average, Bayesian analysis is a good reflection of the data.

Figure 5. Comparison between physical lens system properties $M_L$ and $D_{\text{LS}}$ from Bayesian analysis and those derived from the parallax measurements, for Spitzer lenses with unique, unambiguous solutions. For the most part, there is good agreement.

We note that, for OB161195, the physical properties derived from parallax are $M_L = 0.078^{+0.016}_{-0.012}M_\odot$ and $D_L = 3.91^{+0.42}_{-0.46}$ kpc $\rightarrow D_{\text{LS}} \sim 4.29$ kpc, (Shvartzvald et al. 2017). This is between the 68% and 95% CI of both our Bayesian posterior ($M_L = 0.21^{+0.26}_{-0.11}$ and $D_{\text{LS}} = 2.15^{+1.51}_{-1.04}$ kpc), which is based on the $t_E$ and $\theta_E$ given in Shvartzvald et al. (2017), as well as that of Bond et al. (2017), which yielded $M_L = 0.37^{+0.38}_{-0.21}$ and $D_L = 7.20^{+0.85}_{-1.02}$. The discrepancy between our work and that of Bond et al. (2017) is likely due primarily to differences in the Galactic models assumed. An important caveat is that OB161195 is kinematically peculiar: despite its disklike distance, its motion is not in the direction of the disk’s rotation (Shvartzvald et al. 2017). For a Bayesian analysis based on $\theta_E$ and $t_E$, the direction
of the motion would be unknown. However, with this knowledge we recognize that a Bayesian analysis may not accurately reflect the properties of OB161195.

6. THE GALACTIC DISTRIBUTION OF SPITZER BINARY LENSES

Ultimately, the Spitzer planetary systems will be analyzed to determine whether or not planet occurrence varies across the Galaxy. One way to do this is to compare the distance distribution of planetary lenses to that of the Spitzer single-lens sample (Calchi Novati et al. 2015a; Zhu et al. 2017). Note that Penny et al. (2016) undertook a related study, in which they compared ground-based planet discoveries with a simulated host population.

While the Spitzer planet sample is not yet large enough to perform this test, the number of Spitzer 2-body lenses (both planets and binaries) is now comparable to the total number of planets expected for the full Spitzer sample. Thus, we can use the Spitzer binaries to illustrate the methodology for comparing distance distributions. To date, 12 binary lenses from Spitzer have published parameters with unambiguous or strongly preferred solutions, and therefore \( D_{8.3} \) (Table 4). In this count we excluded OB151212 (Bozza et al. 2016) because only 3/8 degenerate solutions have constrained \( D_{8.3} \). We also discarded OB150196 (Han et al. 2017) and OB170329 (Han et al. 2018) because they have severe discrete degeneracies.

Figure 7 shows the empirical binary cumulative distance distribution function for these 12 events. Note that, although OB151319 (Shvartzvald et al. 2016b) was excluded from the Bayesian exercise because its 8 degenerate solutions span primary masses of 0.53 to 0.67 \( M_\odot \) and fail our criteria for mass consistency, it is included here as one entry (with \( D_{8.3} \) of the solution with the best \( \chi^2 \) because the \( D_{8.3} \) for all degenerate solutions are actually all consistent with each other. The substel-

Table 5. Spitzer Parallax-Bayesian Comparison

| Object Abbrv | Parallax \( M_{\text{prim}}(M_\odot) \) | \( D_{\text{LS}} \) (kpc) | Bayesian \( M_{\text{prim}}(M_\odot) \) | \( D_{\text{LS}} \) (kpc) |
|--------------|----------------------------------|-----------------|----------------------------------|-----------------|
| OB140124     | 0.90 ± 0.05                      | 4.28 ± 0.20     | 0.83 ±0.43                       | 5.32 ±1.39     |
| OB140289     | 0.52 ± 0.04                      | 4.73 ± 0.16     | 0.80 ±0.42                       | 4.93 ±1.34     |
| OB140962     | 0.20 ± 0.01                      | 0.41 ± 0.02     | 0.07 ±0.12                       | 1.38 ±0.77     |
| OB141150     | 0.99 ± 0.28                      | 4.23 ± 0.57     | 0.87 ±0.35                       | 4.65 ±1.12     |
| OB150020     | 0.60 ± 0.03                      | 6.21 ± 0.07     | 0.95 ±0.60                       | 5.43 ±1.64     |
| OB150479     | 1.01 ± 0.25                      | 5.98 ± 0.45     | 0.87 ±0.60                       | 5.66 ±1.70     |
| OB150763     | 0.50 ± 0.03                      | 1.28 ± 0.07     | 0.44 ±0.33                       | 2.06 ±1.41     |
| OB150966     | 0.39 ± 0.04                      | 4.76 ± 0.19     | 0.80 ±0.44                       | 4.21 ±1.20     |
| OB151268     | 0.05 ± 0.01                      | 1.83 ± 0.35     | 0.11 ±0.17                       | 1.24 ±0.66     |
| OB160168     | 0.27 ± 0.03                      | 6.98 ± 0.14     | 0.92 ±0.59                       | 5.34 ±1.43     |
| OB161045     | 0.08 ± 0.01                      | 3.86 ± 0.15     | 0.26 ±0.35                       | 2.19 ±1.05     |
| OB161190     | 0.88 ± 0.08                      | 1.62 ± 0.13     | 0.71 ±0.28                       | 2.79 ±1.42     |
| OB161195     | 0.07 ± 0.01                      | 4.29 ± 0.38     | 0.21 ±0.26                       | 2.15 ±1.04     |

Notes:

\( ^a \): Bayesian values shown are median and symmetric 68% CIs.

Figure 6. Empirical cumulative distribution function of Bayesian posterior fraction above the lens system's physical properties (\( M_L \) and \( D_{\text{LS}} \)) derived from parallax, for Spitzer lenses with unique, unambiguous solutions. The distributions are consistent with 1-to-1, suggesting that the Bayesian posteriors are a fair representation of the underlying true parameters.
Figure 7. Top Panel: The empirical cumulative distance distribution function of Spitzer binary lenses (black), overlaid on the Spitzer single lens detections from 2015 (red). The binary ensemble has only a 2.5% probability of being drawn from the single lens distribution. Bottom Panel: The cumulative distribution of $t_E$ for single lenses (red) and binary lenses (black), with the distribution of $t_E$ calculated from the primary component of the binary lens denoted by the black solid line. Based on a 2-sample KS test, the single and binary lens distributions are discrepant at the 3σ level.

This visual discrepancy, we perform a 1-sample KS-test for the empirical CDF. Formally, at a p-value of 0.025, the null hypothesis that the binary and single lens sample are drawn from the same distribution can be rejected at 2σ significance.

Investigating the source of this intermediate-distance excess relative to the bulge is outside the scope of this paper, since any physical conclusions would first require disentangling the contribution from selection effects. While the selection effects should be the same for planets compared to single lenses, this is not necessarily true for binaries (cf. Yee et al. 2015b). For example, some binaries are discovered serendipitously as part of the single-lens sample selected for Spitzer followup, whereas others are deliberately observed by Spitzer after their binary anomalies are already detected from the ground. One indication of possible selection bias between single and 2-body Spitzer lenses is displayed in the bottom panel of Figure 7, which shows a 3σ discrepancy (from a 2-sample KS test) between the $t_E$ distributions of single and binary lenses. The Figure gives the $t_E$ directly from the model (which is relative to the total mass of the system) and the $t_E$ relative to the primary alone. The latter is the most relevant comparison for single lenses because it shows what would have been observed in the absence of a companion. The discrepancy in the $t_E$ distribution likely contributes to the excess at intermediate distances, but even the origin of the $t_E$ discrepancy is unknown (possibly related to selection effects). Regardless of the physical explanation for the excess at 3 – 5 kpc, the above analysis shows that this method can measure significant differences in the distance distribution of a population with only 12 objects relative to the single-lens population.

7. SUMMARY

Measurements of the Einstein radius ($\theta_E$) and the microlens parallax ($\pi_E$) make a powerful combination for deducing the physical properties of lensing systems, such as mass, distance, and kinematics. This information is readily available for events involving binary lenses with satellite observations. However, for many ground-based microlensing discoveries it is not possible to obtain both quantities for an unambiguous solution. In these cases, a Bayesian analysis, based on a Galactic model, is used to give a probabilistic estimate of the physical parameters. The interpretation of many individual systems and ensemble statistics depends on the accuracy of the Bayesian analysis, which we systematically verify in this work.

We first present the discovery and characterization of OGLE-2014-BLG-0962 using high quality ground-based
survey and Spitzer data. The densely covered light curves allow us to constrain $\theta_E$ and $\vec{\pi}_E$ very well, leading to a unique interpretation of this object to be a textbook mid-M-M stellar binary deeply embedded in the Galactic bulge. However, the angular Einstein radius (0.14 mas) is on the low side. Thus, if we were to infer the physical properties of this system without using the parallax information – that is, using a standard Bayesian analysis based on a Galactic model prior – we would infer a much lower lens mass.

To investigate whether the Bayesian framework is on average reliable, we assemble a sample of 13 well-understood Spitzer systems and perform Bayesian analysis on each of them using their $t_E$ and $\theta_E$ as inputs. We compare the Bayesian predictions of lens mass ($M_L$) and lens-source distance ($D_{LS}$) to the same physical properties calculated from $\pi_E$, finding good agreement overall and concluding that the Bayesian posteriors are on average representative of the true answers.

We also construct a sample of Spitzer binaries and show the methodology for making quantitative statements about the Galactic distribution of planetary and binary lenses using detections from Spitzer. A comparison with that of single lens detections from Spitzer shows tentative evidence that the two types of lenses are drawn from incompatible distance distributions. Specifically, binaries may be more abundant relative to single stars at the intermediate distances (i.e. 3–5 kpc) and deficient beyond $\sim$ 6 kpc, the latter coinciding with the geographical location of the Galactic bulge. We do not investigate the reason for this discrepancy, which could be related to the difference in the $t_E$ distributions or other selection effects. However, while understanding the exact source of this excess lies outside the scope of this work, we have demonstrated our ability to measure a significant difference between a reference spatial distribution function and that of a sample of interest with just 12 objects. Our finding bodes well for the primary mission of the Spitzer microlensing campaign to constrain the Galactic distribution of planets using a similarly sized sample.

ACKNOWLEDGMENTS

The authors would like to thank John Johnson, Jason Eastman, and other members of the Exolab for providing helpful suggestions and feedback throughout the course of this work. We are grateful to Vinay Kashyap for his statistical guidance. We thank Wei Zhu for contributing the data for the Spitzer single lens CDF (i.e., Figure 12 of Zhu et al. (2017)) and for discussions. Y. Shan is supported in part by a Doctoral Postgraduate Scholarship from the Natural Science and Engineering Research Council (NSERC) of Canada. The OGLE project has received funding from the National Science Centre, Poland, grant MAESTRO 2014/14/A/ST9/00121 to AU. OGLE Team thanks Profs. M. Kubiak and G. Pietrzyński, for their contribution to the OGLE photometric dataset. The MOA project is supported by JSPS KAKENHI Grant Number JSPS24253004, JSPS26247023, JSPS23340064, JSPS15H00781, and JP16H06287. This research was supported by the I-CORE programme of the Planning and Budgeting Committee and the Israel Science Foundation, Grant 1829/12. DM and AG acknowledge support by the US-Israel Binational Science Foundation.

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