Evidence of Environmental Dependencies of Type Ia Supernovae from the Nearby Supernova Factory indicated by Local Hα

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ABSTRACT

Context. Use of Type Ia supernovae (SNe Ia) as distance indicators has proven to be a powerful technique for measuring the dark energy equation of state. However, recent studies have highlighted potential biases correlated with the global properties of their host galaxies, sufficient in size to induce systematic errors into such cosmological measurements if not properly treated.

Aims. We study the host galaxy regions in close proximity to SNe Ia in order to analyze relations between the properties of SN Ia events and environments most similar to where their progenitors formed. In this paper we will focus on local Hα emission as an indicator of young progenitor environments.

Methods. The Nearby Supernova Factory has obtained flux-calibrated spectral timeseries for SNe Ia using integral field spectroscopy. These observations enable the simultaneous measurement of the SN and its immediate vicinity. For 89 SNe Ia we measure or set limits on Hα emission tracing ongoing star formation within a 1 kpc radius around each SN. This constitutes the first direct study of the local environment for a large sample of SNe Ia also having accurate luminosity, color and stretch measurements.

Results. Our local star formation measurements provide several critical new insights. We find that SNe Ia with local Hα emission are redder by 0.036 ± 0.017 mag, and that the previously-noted correlation between stretch and host mass is entirely driven by the SNe Ia coming from locally passive environments, in particular at the low-stretch end. There is no such trend for SNe Ia having locally star-forming environments. Our most important finding is that the mean standardized brightness for SNe Ia with local Hα emission is 0.094 ± 0.031 mag fainter on average than for those without. This offset arises from a bimodal structure in the Hubble residuals, with one mode being shared by SNe Ia in all environments and the other one being exclusive to SNe Ia in locally passive environments. This structure also explains the previously-known host-mass bias. We combine the star-formation dependence of this bimodality with the cosmic star-formation rate to predict changes with redshift in the mean SN Ia brightness and the host-mass bias. The strong change predicted is confirmed using high-redshift SNe Ia from the literature.

Conclusions. The environmental dependences in SN Ia Hubble residuals and color found here point to remaining systematic errors in the standardization of SNe Ia. In particular, the observed brightness offset associated with local Hα emission is predicted to cause a significant bias in current measurements of the dark energy equation of state. Recognition of these effects offers new opportunities to improve SNe Ia as cosmological probes. For instance, we note that SNe Ia associated with local Hα emission are more homogeneous, having a brightness dispersion of only 0.105 ± 0.012 mag.

Keywords. Type Ia supernovae – progenitors – host galaxies – cosmology : observations – IFS – dark energy

Article number, page 1 of 19
1. Introduction

Luminosity distances from Type Ia supernovae (SNe Ia) were key to the discovery of the accelerating expansion of the universe (Perlmutter et al. 1999; Riess et al. 1998). Among the current generation of surveys more than 600 spectroscopically confirmed SNe Ia are available for cosmological analyses (e.g. Suzuki et al. 2012). Thus, even today SNe Ia remain the strongest demonstrated technique for measuring the dark energy equation of state.

The fundamental principle behind the use of these standardized candles is that the standardization does not change with redshift, SNe Ia have an observed $M_B$ dispersion of approximately 0.4 mag, which makes them naturally good distance indicators. Empirical light-curve fitters such as SALT2 (Guy et al. 2007, 2010) or MLCS2K2 (Jha et al. 2007) correct $M_B$ for the "brighter-slower" and "brighter-bluer" relation (Phillips 1993; Riess et al. 1996; Tripp 1998). This stretch (or $x_t$) and color ($c$) standardization enables the reduction of their magnitude dispersion down to $\approx 0.15$ mag.

However, a major issue remains: despite decades of study, their progenitors are as yet undetermined. (See Maoz & Manucci 2012, for a detailed review). Like all stars, it is expected that these progenitors will have a distribution of ages and metal abundances, and these distributions will change with redshift. These factors in turn may effect details of the explosion, leading to potential bias in the cosmological measurements. The remaining 0.15 mag “intrinsic” scatter in SN Ia standardized brightnesses is a direct indicator that hidden variables remain. Host galaxy dust – and peculiar velocities if the host is too nearby – complicate the picture.

Several studies have found that the distribution of SNe Ia light curve stretches differs across host galaxy total stellar mass (Hamuy et al. 2000;Neill et al. 2009; Sullivan et al. 2010) and global specific star formation rate (sSFR) (Lampeitl et al. 2010; Konishi et al. 2011). Lampeitl et al. (2010) concluded that the distribution of SNe Ia colors appears to be independent of host star-forming properties, even though more dust is expected in actively star-forming environments. Although, in Childress et al. (2013a) we found that SNe Ia colors do correlate with host metallicity; this may be intrinsic, but also metals are a necessary ingredient for dust formation. Stretch is correlated with observed $M_B$, so after standardization the influence of this environmental property disappears.

A dependence of corrected Hubble residuals on host mass is now well-established (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013). This has been modeled as either a linear trend or a sharp step in corrected Hubble residuals between low- and high-mass hosts. In Childress et al. (2013a) we established that a "mass step" at log(M/M$_\odot$) $\approx$ 10.2 gives a much better fit than a line, and we found that the RMS width of the transition is only 0.5 dex in mass. Because the mass of a galaxy correlates with its metallicity, age, and sSFR (see Tremonti et al. 2004; Gallazzi et al. 2005; Pérez-González et al. 2008, respectively), this mass step is most likely driven by an intrinsic SN progenitor variation. For instance, a brightness offset between globally star-forming and globally passive galaxies provides a fair phenomenological description of the mass step (D’Andrea et al. 2011), being driven by the sharp change in the fraction of star-forming hosts at log(M/M$_\odot$) $\sim$ 10 present in the local universe (Childress et al. 2013a).

Though, by analyzing global properties of the host galaxy, the aforementioned analyses are limited in the interpretation of their results. The measured quantities – gas metallicity, star formation rate, etc. – are light-weighted. Thus global analyses are most representative of galaxy properties near the core, which can be significantly different than the actual SN environment. This is illustrated in Fig. 1: inside these two spiral star-forming galaxies, a SN occurred either in an old passive inter-arm environment (SN 2007kk) or inside a star-forming one (SN 2005L).

In this work we analyze the host galaxy regions in the immediate vicinity for a large sample of SNe Ia from the Nearby Supernova Factory (SNFactory, Aldering et al. 2002). Our integral field spectrograph accesses the local environment of observed SNe, and therefore probes local host properties such as gas and stellar metallicities and star formation history. While Stanishev et al. (2012) conducted such a study by looking at the metallicity of the local environments of a sample of seven nearby SNe Ia, ours is the first such large-scale study.

Delay-time distribution studies (Scannapieco & Bildsten 2005; Mannucci et al. 2005, 2006; Sullivan et al. 2006) predict that a fraction of SNe Ia, known as “prompt” SNe, should be associated with young stellar populations. The rest, referred to as “tardy” or “delayed” SNe, should be related to older stars. Individual star-forming regions (H ii regions) have a typical lifetime of a few Myr (Alvarez et al. 2006), much smaller than expected – even for the fastest – SN Ia progenitor systems (few tens of Myr, Girardi et al. 2000). It is therefore impossible to make a physical connection between a SN and the H ii region in which its progenitor formed. However such star forming regions are gathered in groups (see for instance M 51 in Lee et al. 2011), concentrated in spiral arms whose lifetimes are longer than the time scale for a prompt SN. (See Kauffmann et al. 2003, for details on the star formation history).
formation history of galaxies.) This motivated us to employ Hα for our first analysis of SNe Ia local environments. Hα will be taken to indicate active local star formation, and the likelihood that a given progenitor was especially young.

Long before the “prompt” and “tardy” distinction, association with Hα regions or spiral arms was a common approach for understanding the stellar populations from which SNe Ia formed. For instance, with small samples of SNe, Bartunov et al. (1994) and later James & Anderson (2006) showed that type Ia SNe were less associated with such regions than are core-collapse SNe. A key ingredient missing in such studies needed to understand SNe Ia in detail is accurate standardized luminosities, which we have for our sample. Also, in light of the “prompt”/”tardy” dichotomy, it will be important to consider the possibility that SNe Ia will fall into discrete subsets based on the strength of star formation in their local environment.

After the presentation of our data (Sect. 2) and our method for quantifying neighboring star-forming activity (Sect. 3), we investigate the correlation of SNe Ia light-curve parameters with the local environment (Sect. 4). This includes a review of how to properly measure light-curve parameters, including quality cuts suggested by Guy et al. (2010).

2.2. Local Host Observations

The SNfactory software pipeline provides flux calibrated $x, y, \lambda$-cubes corrected for instrumental and atmospheric responses (Buton et al. 2013). Each spaxel of an SN cube includes three components, each one characterized by its own spatial signature:

1. the SN is a pure point source, located close to the center of the SNIFS field of view (FoV);
2. the night sky spectrum is a spatially flat component over the full FoV;
3. the host galaxy is a (potentially) structured background.

In this section, we present the algorithm used to disentangle the three components. In Sect. 2.2.1, we describe the method used to subtract the SN component from the original cubes, and in Sect. 2.2.2 our sky subtraction procedure, using a spectral model for the sky that prevents host-galaxy signal contamination. All cubes from the same host are finally combined to produce high signal-to-noise (S/N) cubes and spectra; this process is detailed in Sect. 2.2.3.

2.2.1. SN Subtraction

The point source extraction from IFS data requires the proper subtraction of any structured background. Using a 3D deconvolution technique, Bongard et al. (2011) show how we construct a “seeing-free” galaxy $x, y, \lambda$-cube from final reference exposures taken after the SN Ia has vanished (typically one year after maximum light). This model, after proper registration and re-convolution with the appropriate seeing, is subtracted from each observed cube to leave the pure point-source component plus a spatial constant similar to a sky signal. Three dimensional PSF photometry is then applied to the host-subtracted cube to extract the point source spectrum (e.g. Buton et al. 2013).

For the present local host property analysis, we went one step further and subtracted the aforementioned fitted PSF from the original cubes to obtain SN-subtracted host cubes. Figure 2 shows an example of such a subtraction procedure. Since the SNfactory acquires SNe Ia time series, this technique provides as many local host observations as SN pointings (on average 13), in addition to the final references (on average 2).

2.2.2. Sky Subtraction

Since SNIFS has a FoV spanning only $\sim 6''$ across, it is usually not possible to find a region entirely free of host signal, as is usually done in photometry or long-slit spectroscopy. The night sky spectrum is a combination of the atmospheric molecular emission, zodiacal light, scattered star light, along with the moon contribution if any (Hanuschik 2003). We have developed a sky spectrum model from a principal component analysis (PCA) on 700 pure sky spectra obtained from standard star exposures in various observing conditions. The B and R channels are analyzed independently and in slightly different ways.

The emission lines in R sky spectra (mainly oxygen and OH bands) are easily isolated from the underlying continuum. This continuum is fitted by a 4th-order Legendre polynomial over the explosion to serve as a final reference to enable the subtraction of the underlying host. For this analysis, we have gathered a subsample of 119 SNe Ia with good final references and properly measured light-curve parameters, including quality cuts.
emission line-free wavelength regions. The PCA is then performed on the continuum-subtracted emission line component. Eight principal components (PCs) are necessary to reconstruct the emission spectrum with a median reduced $\chi^2$ of 1. An example of a red-sky spectrum fit using this 13-parameter model is given in Fig. 3.

The $B$ sky spectrum is dominated by diffuse light and shows absorption features, as well as a few Herbig O2 lines in the bluer part of the spectrum. For this channel a PCA is performed directly on the observed sky spectra, since it was not possible to disentangle the different physical components as easily as for the $R$ sky spectra. We find that four PCs are necessary to reach a median reduced $\chi^2$ of 1.

In total, our $B + R$ sky model is therefore described by $4 + (5 + 8) = 17$ linear parameters. Since this model is trained on selected pure sky spectra, none of the PCs should mimic galactic features: even if some chemical elements are common (e.g. the hydrogen or nitrogen lines), host galactic lines are redshifted, and cannot be spuriously fit by the model.

Each spaxel of the SN-subtracted cube can be decomposed as follows:

$$\text{spaxel}(x, y, \lambda) = \text{host}(x, y, \lambda) + \text{sky}(\lambda),$$

where the spatially flat sky component does not depend on the spaxel location $(x, y)$. We define the presumed sky as the mean spectrum of the 5 faintest spaxels, i.e. with the smallest host contribution. Since the host$(x, y, \lambda)$ component of Eq. 1 may not be strictly null for these spaxels, the presumed sky may still contain galactic features, e.g. hydrogen emission lines, and cannot be used directly as a valid estimate of the true sky spectrum. We therefore fit the presumed sky spectrum with our model: the resulting modeled sky is free from any galactic features, and can safely be subtracted from each spaxel to obtain a pure host cube. (See Fig. 3 for an example on $R$-channel.)

This procedure could slightly overestimate the sky continuum in cases of bright host signal even in the faintest spaxels, and ultimately lead to a under-estimation of the Hα flux measurements (Groves et al. 2012). This effect is however insignificant in comparison to our main source of Hα measurement error, related to our inability to correct for host dust extinction (see Sect. 2.3).

2.2.3. Spectral Merging

In this analysis, we focus on the host properties of the SN local environment, which we define has having projected distances less than 1 kpc from the SN. This radius was chosen since it is greater than our median seeing disk for our most distance host galaxies, at $z = 0.08$. (1″ = 1.03 kpc at $z = 0.05$.) No allowance is made for host galaxy inclination in defining this local region.

Once the SN and the sky components have been subtracted, we compute from each cube the mean host spectrum within 1 kpc around the SN. This requires precise spatial registration (a by-product of the 3D deconvolution algorithm, see Sect. 2.2.1) and atmospheric differential refraction correction. Those spectra (15 on average per SN) are then optimally averaged and merged to get one host spectrum of the local environment per SN. The spectral sampling of these merged-channel spectra is set to that of the $B$-channel, i.e. 2.38 Å. In the same fashion, we are able to combine 3D-cubes to create 2D-maps of any host property.

The spectra are corrected for Milky-Way extinction (Schlegel et al. 1998). In this paper, observed fluxes are expressed as surface brightnesses, and wavelengths are shifted to rest-frame. We only consider the 89 SNe Ia in the main SNfactory redshift range $0.03 < z < 0.08$ for spatial sampling reasons. Namely, at lower $z$ the final SNIIFS field of view remaining after spectral merging often subtends a radius of less than 1 kpc surrounding the SN location, while at higher $z$ the typical seeing disk subtends substantially more than 1 kpc. Since this selection is based on redshift only, it does not introduce bias with respect to host or SN Ia properties. (See Childress et al. 2013b, who showed that our host data follow regular galaxy characteristics.)

The influence of the PSF, i.e. the variation of the amount of independent information with redshift for a given kpc-radius...
aperture, is discussed in Sect. 7, where we show that our analysis is free from any redshift bias.

2.3. Measurement of the Local Host Properties

A galactic spectrum is a combination of a continuum component with absorption lines mostly from the stars, and emission lines from the interstellar gas. In this paper, we restrict our analysis to the Hα signal around the SN. Since hydrogen emission line intensities can be affected by underlying stellar absorption, it is necessary to estimate the stellar continuum to obtain accurate Hα measurements. (See Fig. 4.)

The University of Lyon Spectroscopic analysis Software1 (ULySS, Koleva et al. 2008, 2009) is used to disentangle the stellar and gas components. It fits simultaneously the following three components: stellar populations from the MILES library (Sánchez-Blázquez et al. 2006); a set of emissions lines – Balmer’s hydrogen series in addition to [O ii]λ3726, 3728, [O iii], [N ii] and [S ii]; and a multiplicative ad hoc continuum correcting for both internal dust extinction and any remaining large-scale flux mismatch between the data and the template library. Only wavelengths matching the MILES library rest-frame are considered (3540–7410 Å), and gas emission lines all share a common redshift and velocity dispersion. Because of this added constraint, gas emission flux uncertainties given by ULySS cannot be trusted readily. We therefore ultimately fit gaussian profiles on stellar-corrected emission lines to derive Hα fluxes and accurate uncertainties.

Figure 4 presents the fit of the mean spectrum of the local environment for SNF20060512-001. In this particular case 21 exposures per channel, including two final references, have been combined. The stellar component is strongly constrained by the D4000 feature, and thereby gas flux measurements properly account for stellar absorption.

1 http://ulyss.univ-lyon1.fr

In this paper, we focus our study on the Hα line as a tracer of the star-forming activity (Kennicutt 1998). The spectra are not corrected for the internal host extinction, because the Balmer decrement method (Calzetti et al. 1994) cannot be reliably applied: the Hγ lines are usually too faint, and Hβ lines happen to lie at the SNIFS dichroic cross-over (4950 < λ < 5150 Å in the observer frame, see Fig. 4), where the S/N is low and fluxes harder to calibrate.

3. Local Hα surface brightness analysis

The Hα emission within a 1 kpc projected radius can be conventionally recast as a surface brightness, which we will designate with ΣHα. Because the measurement is projected, it actually represents the total Hα emission in a 1 kpc radius column passing through the host galaxy centered on the SN position. Thus, it is possible that Hα we detect, in whole or in part, is in the foreground or background of the 1 kpc radius sphere surrounding the SN.

However, there are several factors that greatly suppress projection effects for Hα relative to stars. One is that Hα depends on the square of the electron density, so most Hα comes from those rare regions with high gas density. This advantage is compounded by the fact that young stars capable of ionizing hydrogen also occur preferentially in clumps and regions of higher gas density. (see Kennicutt & Evans 2012, especially section 2.2, for a detailed discussion of H α regions and their clumpiness). In addition, while stars are spread across thin and thick disks, bulges and halos, Hα regions are concentrated in the thin galactic disk, where a typical scale height is only ~ 0.1 kpc (Paladini et al. 2004). Thus the line-of-sight depth extends beyond our canonical 1 kpc radius only for very high inclinations (i.e., i > 84 deg). Finally, the Hα covering fraction is generally small because H α regions are so short-lived (see Calzetti 2012, for a detailed review of tracers of star formation activity.)

In the following analysis, a few cases (7/89) of SNe with locations projected close to the core of very inclined hosts have been set aside because of the high probability of such misassociation (designated as “p.m.s.”, see Table 1). In Sect. 7 we show that these cases have no influence on our results.

A different projection effect occurs if SNe Ia travel far from their formation environment before they explode. Due to random stellar motions this will occur, and its importance will itself depend on SNe Ia lifetimes and the host velocity dispersion. If as expected, tardy SNe Ia are associated with old stellar populations, this correspondence may be lost only in cases where the host is globally star forming – i.e. for spiral rather than elliptical galaxies – and the SN motion has projected it onto a region of active star formation. As with the line-of-sight projection discussed above, this situation should be uncommon. On the other hand, prompt progenitors should not have drifted from their stellar cohort by more than our fiducial 1 kpc radius. This cohort is likely to have been an open cluster or OB association; open clusters remain bound on the relevant timescale, while OB associations have very low velocities dispersions (~ < 3 km s⁻¹) de Zeeuw et al. 1999; Portegies Zwart et al. 2010; Röser et al. 2010). Consequently, there should be little contamination due to this type of projection effect for young progenitors.

Thus, the net effect will be that for some old SN progenitors in globally star-forming galaxies a false positive association with Hα may arise due to these projection effects. However, we expect the number of such cases to be small, as discussed later in this section.
For ease in interpretation, we split our sample in two, using the median $\Sigma_{H\alpha}$ value of our distribution, $\log(\Sigma_{H\alpha}) = 38.35$, as the division point. This corresponds to a star formation surface density of $1.22 \times 10^{-3} M_\odot$ yr$^{-1}$ kpc$^{-2}$ assuming Eq. 5 of Calzetti et al. (2010). Cases where no H$\alpha$ signal was found are arbitrarily set to $\log(\Sigma_{H\alpha}) = 37$ in the figures.

The median $\Sigma_{H\alpha}$ value happens to correspond to the threshold at which we achieve a minimal 3$\sigma$-level measurement sensitivity. It also corresponds to the mean $\log(\Sigma_{H\alpha})$ of the warm interstellar medium (WIM) distribution reported by Oey et al. (2007). The source of the WIM is controversial. The long-standing interpretation has been that the WIM is due to Lyman continuum photons that have escaped from star-forming regions and then ionize the ISM. In this interpretation the WIM would still trace star formation, but its distribution would be more diffuse than an H$\alpha$ region. This distinction would not matter given our large metric aperture since even in the ISM the optical depth to Lyman continuum photons is large. Recently, however, Seon & Witt (2012) have interpreted the WIM as due to reflection of light from H$\alpha$ regions off of ISM dust. In this case WIM H$\alpha$ would still arise from star formation, but possibly from distances well outside our metric aperture since the optical depth to H$\alpha$ photons can be low. By setting our division point above the nominal $\log(\Sigma_{H\alpha})$ of the WIM we minimize the importance of these details for our analysis.

We designate these two $\Sigma_{H\alpha}$ subgroups as follows (see Table 1):

- 41 SNe Ia$\alpha$ with $\log(\Sigma_{H\alpha}) \geq 38.35$, which we refer to as “locally star forming”;
- 41 SNe Ia$\epsilon$ with $\log(\Sigma_{H\alpha}) < 38.35$, which we refer to as “locally passive”.

Figure 5 presents a quantitative picture of the point made visually in Fig. 1 by illustrating the non-trivial relationship between local and global measurements for cases considered passive. The global quantities for our hosts are taken from our compilation in Childress et al. (2013b); in three cases global SFR measurements are unavailable for SNe Ia in our local environment sample. Figure 5 shows that half of the SNe with locally passive environments (20/38) have a globally star-forming host (traditionally defined as $\log(sSFR) > -10.5$). This highlights the existing degeneracy when employing global properties: the SNe Ia hosted in globally star-forming galaxies can have either star-forming or passive local environments whereas SNe hosted in globally passive galaxies are almost certain to have a locally passive environment.

SNe Ia$\alpha$, having $\Sigma_{H\alpha}$ above the median value, are most likely to have young progenitors since an H$\alpha$ signal has been positively detected in their vicinities. The large number of SNe Ia with detections of local star formation in Fig. 5 itself provides an indication that young progenitors exist, in agreement with the statistical analysis of Aubourg et al. (2008). On the other hand, the wide range of observed $\Sigma_{H\alpha}$ is an indication of SNe from both passive and star-forming regions, i.e. from both young and old progenitors (Scannapieco & Bildsten 2005; Mannucci et al. 2005, 2006; Sullivan et al. 2006).

In Fig. 5 there is a relative dearth of SNe Ia with H$\alpha$ detections for $\log(\Sigma_{H\alpha}) < 37.9$ in hosts that are globally star-forming. This then highlights a population having 38.0 < $\log(\Sigma_{H\alpha})$ < 38.35 in globally star-forming hosts which are counted as locally passive when we split our sample. Their proximity to the typical WIM level suggests that these could be cases of SNe Ia from old progenitors whose $\Sigma_{H\alpha}$ value is boosted by projection onto the WIM in their hosts. But, they equally well may be SNe Ia from young/intermediate age progenitors where strong star formation has already ebbed at that location in their host. In Sect. 7 we show that moving these cases into the star-forming sample does not change our results significantly. Therefore we prefer to employ a simple split since it is not tuned to any patterns in the data.

4. $\Sigma_{H\alpha}$ and SN Ia Light-Curve Properties

We will now compare $\log(\Sigma_{H\alpha})$ to the SN light-curve parameters (Sect. 4.1) and to the corrected Hubble residuals $\Delta M_B^{corr}$ (Sect. 4.2). We show that SNe from locally passive regions have faster light curve decline rates, that the color of SNe Ia is correlated with $\Sigma_{H\alpha}$, and that there is a significant magnitude offset between SNe from locally star-forming (Ia$\alpha$) and locally passive (Ia$\epsilon$) regions.

The SALT2 lightcurve parameters $c$ and $x_1$ are known to correlate with the uncorrected absolute $B$-magnitude at maximum light, $M_B$. The dispersion in $M_B$ can be reduced significantly by taking advantage of these correlations (Guy et al. 2007):

$$\Delta M_B^{corr} \equiv (M_B - \langle M_B \rangle) + (a x_1 - b),$$

where the stretch coefficient $a$, the color coefficient $b$, and the average absolute magnitude of the SNe Ia, $\langle M_B \rangle$, are simultaneously fit over the SN sample during the standardization process. The SALT light curve parameters and Hubble residuals for our SNe Ia have been presented previously in Bailey et al. (2009), Chotard et al. (2011), and Childress et al. (2013a).

For the statistical analyses that follow we will use the Kolmogorov-Smirnov test (KS-test) to estimate the discrepancy between observed parameter distributions ($x_1$, $c$, and $\Delta M_B^{corr}$). We also will compare the weighted-mean values of those distributions between the $\Sigma_{H\alpha}$ groups, which we denote using the form $\delta(X)(A - B) \equiv \langle X \rangle_A - \langle X \rangle_B$. When exploring correlations we will employ the non-parametric Spearman rank correlation...
Table 1. Definition of the two $\Sigma_{H\alpha}$ subgroups, and their respective weighted mean light-curve parameters. The “p.m.s.” column indicates the number of SNe with a potential misassociation of a H$\alpha$ detection due to projection effects, which have been excluded from the main analysis.

| Label | Group                  | $\log(\Sigma_{H\alpha})$ | SNe | $\langle x_1 \rangle$ | $\langle c \rangle$ | $\langle \Delta M^*_{B} \rangle$ [mag] | p.m.s. |
|-------|------------------------|---------------------------|-----|------------------------|-------------------|-----------------------------------|--------|
| Iae   | Locally passive        | $<-38.35$                 | 41  | $-0.29 \pm 0.14$       | $0.029 \pm 0.010$ | $-0.039 \pm 0.023$               | 2      |
| Iaa   | Locally star-forming   | $\geq 38.35$              | 39  | $+0.08 \pm 0.10$       | $0.065 \pm 0.013$ | $+0.056 \pm 0.020$               | 5      |

4.1. Light-Curve Stretch and Color

The stretch parameter $x_1$ and color $c$ are shown in Fig. 6 as a function of $\log(\Sigma_{H\alpha})$. The weighted means and dispersions for the two subgroup are summarized in Table 1.

4.1.1. The Light-Curve Stretch

The SALT2 stretch $x_1$ and the $\log(\Sigma_{H\alpha})$ values are correlated, as evidenced by a highly significant Spearman rank correlation coefficient: $r_s = 0.42$, $p_s = 7.4 \times 10^{-7}$, 4.2$\sigma$. This shows that SNe Ia from low $\Sigma_{H\alpha}$ environments have on average faster light-curve decline rates. When comparing $\Sigma_{H\alpha}$ subgroups, we find $\delta(x_1)(\text{Ia}e - \text{Ia}a) = 0.37 \pm 0.17$ ($p_{KS} = 5.8 \times 10^{-5}$).

At first this might appear to be just the same as the well-established effect whereby globally passive galaxies are found to host SNe Ia with lower stretch while star-forming host galaxies dominate at moderate stretches (Hamuy et al. 2000; Neill et al. 2009; Lampeitl et al. 2010). Indeed, the $x_1$ distributions of SNe in globally passive and in globally star-forming hosts ($\log(sSFR) \leq -10.5$) differ significantly, having $p_{KS} = 2.0 \times 10^{-3}$ for the SNfactory and $p_{KS} = 10^{-7}$ for SDSS (Lampeitl et al. 2010). We compare in Fig. 7 the global and local pictures in the $(c,x_1)$ plane. These two figures can be compared to Fig. 2 of Lampeitl et al. (2010) for the SDSS sample.

However, our analysis of the local environment displays quite a different stretch distribution for passive environments. We find that 40% of SNe that are locally passive have moderate stretches. This is in strong contrast to global analyses. For our SN sample only 25% of globally passive hosts have SNe Ia with lower stretch while star-forming host galaxies evolve with redshift, thus creating a redshift-dependence on the average SNe Ia luminosity. Distance measurements to these standardizable candles are therefore biased. A more complete discussion of the potential impact on cosmological measurements is presented in Sect. 6.

In summary, we find that lower stretch SNe Ia are hosted almost exclusively in passive local environments, but that SNe Ia having moderate stretches are hosted by all types of environments.

4.1.2. The Light-Curve Color

We also find that SNe Ia from star-forming environments are on average redder than those from passive environments at the 2.2$\sigma$ level: $\delta(c)(\text{Ia}e - \text{Ia}a) = 0.036 \pm 0.017$ ($0.031 \pm 0.015$ when removing the reddest, SNF20071015-000). This effect is more significant when comparing the tails of the $\log(\Sigma_{H\alpha})$ distribution (lower and upper quartiles), where we find distribution differences with $p_{KS} = 0.026$.

As seen in Fig. 6, the SALT2 color, $c$, and the $\log(\Sigma_{H\alpha})$ values are correlated, with a 2.0$\sigma$ non-zero Spearman rank correlation coefficient $r_s = 0.21$, with $p_s = 0.054$.

Since dust is associated with active star formation (e.g. Charlot & Fall 2000), a color excess is expected for SNe Ia in strong $\Sigma_{H\alpha}$ environments. (See Chotard et al. 2011, for a discussion of the Type Ia color issue.) This trend has been suggested for SNLS SNe in Sullivan et al. (2010) but is not seen in SDSS data (Lampeitl et al. 2010).

As discussed earlier, by analyzing integrated galaxy properties, global host studies merge SNe Iae with $x_1 > -1$, and the SNe Ia into a single star-forming host category. Figure 7 shows that low and moderate stretch Iae share the same color distribution. It is then difficult for global analyses to detect the color variation between the globally star-forming and passive hosts, since both kinds harbor some Iae. Indeed, in the SNfactory sample globally passive and globally star-forming hosts produce SNe Ia having the same SALT2 color distribution ($p_{KS} = 0.654$).

4.2. Hubble Residuals

The SALT2 raw Hubble residuals $\Delta M_B$ are corrected for their stretch and color dependencies ($\Delta M^*_{B}$) and are shown in Fig. 6 as a function of $\log(\Sigma_{H\alpha})$. The weighted mean values per $\Sigma_{H\alpha}$ group are summarized in Table 1.

4.2.1. The H$\alpha$ bias

We find with a 3.1$\sigma$ significance that SNe from locally passive environments are brighter than those SNe Ia in locally star-forming environments after color and stretch correction: $\delta(M^*_{B})(\text{Ia}e - \text{Ia}a) = -0.094 \pm 0.031$ mag ($p_{KS} = 0.012$). The amplitude of this significant brightness offset – hereafter called the “H$\alpha$ bias” – is a concern for precision cosmology, since the fraction of SNe Ia from passive environments most likely evolves with redshift, thus creating a redshift-dependence on the average SNe Ia luminosity. Distance measurements to these standardizable candles are therefore biased. A more complete discussion of the potential impact on cosmological measurements is presented in Sect. 6.
This leads us to investigate the possible origin of the brightness offset between the SNe Iaα and the SNe Iaε (Hα bias) by examining the ΔM_B^{corr} distributions of each subgroup. In Fig. 6 we notice the presence of a subgroup of significantly brighter SNe hosted exclusively in locally passive environments. We thus distinguish two modes in the distribution of corrected Hubble residuals: (1) The first mode exists in all environments and has ΔM_B^{corr} ≥ 0. (2) The second mode is exclusive to SNe Ia from low Hα environments (Iaε) and populates the brighter part of the diagram almost exclusively: among the 20 SNe Ia with ΔM_B^{corr} < -0.1, 17 are Iaε, and only one has a log(ΣHα) > 39. For analysis purposes we will define and label these modes as follows:

- **Mode 1 (M1)**: 65 SNe consisting of all SNe Iaα along with SNe Iaε that have ΔM_B^{corr} > -0.1 mag.
- **Mode 2 (M2)**: 17 SNe Iaε with ΔM_B^{corr} < -0.1 mag.

Except for the fact that both are from locally passive environments, the M2 subgroup and the subgroup of 15 fast declining (x1 < -1) SNe Ia turn out to not be directly related, having only 6 SNe in common.

Figure 8 shows the distribution of these two modes fitted by normal distributions (with 3σ clipping). M1 SNe are on average fainter (⟨ΔM_B^{corr}⟩_{M1} = 0.072 ± 0.012 mag) and M2 SNe Ia are brighter (⟨ΔM_B^{corr}⟩_{M2} = -0.191 ± 0.015 mag) than the full sample. The standard deviations are 0.099 ± 0.009 mag and 0.060 ± 0.010 mag for M1 and M2, respectively. The weighted RMS gives similar results, with variations at a tenth of the error level. With no clipping, one additional, bright SN is then retained in M1, raising the M1 standard deviation to 0.113 ± 0.010 mag.

These differences in ΔM_B^{corr} would appear to be extremely significant. However in this case we chose the dividing point in ΔM_B^{corr} and thus the added degrees of freedom are not accounted for. To better assess the significance of the bimodal structure we...
use the Akaike Information Criterion corrected for finite sample size (AICc; Burnham & Anderson 2002). When comparing two models, the one with the smallest AICc provides a better fit to the data. The AICc test is similar to a maximum likelihood ratio test that penalizes additional parameters.

The two models that we compare are the following: (1) The reference model is a regular normal distribution, with two parameters – a mean and an intrinsic dispersion. (2) The alternative model is bimodal with three parameters – two means and the ratio of the two mode amplitudes. In both cases the integral of the model is required to equal the number of SNe used in the fit. For the full sample we find $\Delta$AICc(bimodal - unimodal) = $-5.6$, which strongly favors the bimodal structure. If we remove the possibly-contaminated “p.m.s” cases we find a slightly reduced value of $\Delta$AICc(bimodal - unimodal) = $-4.3$. Thus, whether we include these or not has little impact. The fact that the bimodal model does not require the introduction of an ad hoc intrinsic dispersion lends it further weight.

In addition we have tested for bimodality in the Hubble residuals for the locally passive subset alone. Here the first normal mode is forced to match the mean $\Delta M_c^{corr}$ of the Ia$\alpha$ subset ($\mu_1 = 0.056$) while the mean of second normal mode and the ratio of the two mode amplitudes are free parameters. Here again there is no need to include intrinsic dispersion, thus there are only two parameters. When comparing those two models, $\Delta$AICc(bimodal - unimodal) = $-3.5$, which again favors the bimodal structure, though less strongly.

In Sect. 5.2.2 we will show how this peculiar structure introduces the brightness offset observed between SNe in low- and high-mass hosts. This “mass step” is seen in our sample (Childress et al. 2013a), as well as in all other large surveys (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Johansson et al. 2013). This suggests that this bimodality is not exclusive to the SNefactory data, but is an intrinsic property of SALT2-calibrated SNe Ia. That it has not been noticed before is very likely due to the rarity of SNe Ia having all of the necessary ingredients – well-measured lightcurves, small uncertainties due to peculiar velocities and a wide range of $\Sigma_{H_0}$ and/or total stellar mass.

5. Discussion

In this section, we discuss the results previously presented. First, we look for the potential environmental dependency of stretch and color coefficients among the two $\Sigma_{H_0}$ subgroups (Sect. 5.1). Next, we investigate the previously-observed relations between host masses and both the SNe stretches (Sect. 5.2.1) and the SNe corrected Hubble residuals (Sect. 5.2.2). These relations are interpreted from our local analysis perspective.

5.1. The Standardization Process

In the previous section, the distributions of SN Ia parameters have been shown to vary between our two $\Sigma_{H_0}$ subgroups. In this section, we investigate whether a unique standardization process applies in the context of SALT2, by comparing stretch and color coefficients ($\alpha$ and $\beta$ respectively; see Eq. 2) between the $\Sigma_{H_0}$ subgroups.

We find that the stretch coefficient, $\alpha$, is consistent between $\Sigma_{H_0}$ groups, having $\delta \alpha(Ia \alpha - Iae) = -0.020 \pm 0.037$.

The color coefficient of SNe between low-and high-$\Sigma_{H_0}$ differ by $\delta \beta(Ia \alpha - Iae) = 1.0 \pm 0.41$, but this difference is dominated by the reddest SN, SNF20071015-000. After removing it the color coefficients are not significantly different: $\delta \beta(Ia \alpha - Iae) = 0.67 \pm 0.45$. Therefore, our analysis is insensitive to any color coefficient variations between $\Sigma_{H_0}$ groups. The color of the out-
5.2. Host Mass vs. SN properties: A Local Environment Perspective

We investigate here the correlations found by global host studies, namely between total host stellar mass and both the stretch and the SN corrected Hubble residuals (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013).

5.2.1. The Mass-Stretch Correlation

Stretch has been shown to correlate with host stellar mass (e.g. Sullivan et al. 2010). Figure 9 shows $x_1$ as a function of host mass for our sample (see Childress et al. 2013a, for details on the SNfactory host mass analysis). In agreement with the literature, we find a correlation between mass and stretch when all the SNe Ia are considered together, with a Spearman rank correlation coefficient that is non-zero at the 3.4σ level ($r_s = -0.36, p_s = 9.2 \times 10^{-4}$).

When looking at $\Sigma_{H\alpha}$ subgroups though, we notice that SNe Ia from locally star-forming environments (Ia) show no correlation between their stretch and the mass of their host ($r_s = -0.02 ; p_s = 0.89$). The original correlation is actually driven by SNe Ia from locally passive environments ($r_s = -0.55; p_s = 4.8 \times 10^{-3}$, a 3.0σ significance). More precisely, the correlation appears to arise from the bimodal $x_1$ structure of this subgroup, which we previously noted in Fig. 6. Figure 9 clearly shows that the correlation is related to the L-shaped distribution of SNe Ia in the $x_1$–mass plane: SNe with $x_1 > -1$ contribute to the whole range of host masses, whereas the ones with $x_1 < -1$ arise exclusively in massive galaxies ($\log(M/M_\odot) > 10$).

From the local environment point-of-view, the light-curve widths of SNe in locally star-forming regions are independent of the total stellar mass of their hosts: for SNe I, the total host stellar mass is not a stretch proxy as suggested by Sullivan et al. (2010) but an indicator of whether the two stretch subgroups ($x_1 - 1$) are represented or not. From this new perspective, the mass-stretch correlation shown Fig. 2 of Sullivan et al. (2010) could be re-interpreted as being driven by a relatively independent grouping of SNe having larger masses ($\log(M/M_\odot) > 10.2$) and lower stretches ($s < 0.9 - x_1 < -1$; Guy et al. 2007).

5.2.2. The “Mass Step”

The second known correlation between host masses and SNe Ia properties is a offset in corrected Hubble residuals between SNe hosted by high-mass galaxies (brighter) and those from low-mass hosts (fainter). This can be seen in Fig. 10. This mass effect has been observed by all of the large SNe Ia surveys (Kelly et al. 2010; Sullivan et al. 2010; Gupta et al. 2011; Childress et al. 2013a; Johansson et al. 2013), and compiled in Childress et al. (2013a). Hereafter, we will use the term “plateau” to denote the averaged $\Delta M^\text{corr}$ values for SNe from either high (H) or low-mass (L) galaxies, with a dividing point set at $\log(M/M_\odot) = 10$.

In Childress et al. (2013a) we showed that such a step function is a very good description of the data. The difference in the
brightness of these two plateaus will be referred to as the “mass step.” For our subset of the SNfactory sample this offset reaches \(\delta(M_{B}^{\text{corr}})(H - L) = -0.098 \pm 0.031\) mag.

We notice in Fig. 10 (see also Fig. 2 of Childress et al. 2013a) that the upper part of the envelope of the distribution is constant with mass whereas the lower part of the distribution extends to bright \(\Delta M_{B}^{\text{corr}}\) values for masses above \(\log(M/M_{\odot}) \sim 10\). We see that the high-mass plateau is brighter only because a subgroup of bright SNe exists in massive hosts. A similar trend can be observed in Fig. 4 of Sullivan et al. (2010) for SNLS, in Fig. 15 of Johansson et al. (2013) for SDSS, and in Fig. 5 of Childress et al. (2013a) where we combined all available data.

We see in the top panel of Fig. 10 that the local \(H_{\alpha}\) environment changes with the total host stellar mass. For low masses up to \(\log(M/M_{\odot}) \lesssim 10\), locally star-forming environments dominate (23 Ia/34). In more massive hosts (\(\log(M/M_{\odot}) \gtrsim 10\)), however, the local SN environment presents a marked change and the locally passive cases become favored (27 Ia/45). Since only a few \(M_{2}\) SNe Ia are present in lower mass hosts (3 M2/34), the first plateau happens to be equal to the mean \(M_{1}\) value, with \(\langle \Delta M_{B}^{\text{corr}} \rangle_{L} = 0.066 \pm 0.021\). In the upper mass range, because of the rise of the Iae subgroup populating the brighter \(M_{2}\) mode, the average brightness increases up to the level of the second plateau. The Iae population shows no appreciable mass step; we find \(\delta(M_{B}^{\text{corr}})_{\text{Iae}}(H - L) = -0.06 \pm 0.04\), largely driven by the bright SNF20070701-005. There is a strong possibility that this SN Ia is a false positive \(H_{\alpha}\) association (see Sect. 6.2), and if we remove it we find \(\delta(M_{B}^{\text{corr}})_{\text{Iae}}(H - L) = -0.04 \pm 0.04\). We conclude therefore that the existence of a brighter mode, completely dominated by SNe having locally passive environments, causes both the \(H_{\alpha}\) bias and the mass step.

6. Consequences for Cosmology

The proportion of SNe from locally passive environments has surely changed with time, so the fraction of \(M_{2}\) SNe will be redshift-dependent, and thus we expect the amplitude of the mass step will change as well. In this section we develop a first estimate of this evolution bias and its consequences for measurements of cosmological parameters. In Sect. 6.1, we predict the redshift dependence of the magnitude bias due to evolution in the relative numbers of SNe Ia and SNe Iae given the \(H_{\alpha}\) bias we observe. Using this, we then estimate the bias on measurement of the dark energy equation of state parameter, \(w\), that would result if this evolution does indeed occur. By then coupling the \(H_{\alpha}\) bias and the mass step as discussed in Sect. 6.1.2, we verify the predicted evolution of the mass step using data from the literature. In Sect. 6.2, we introduce a subclass of SNe whose Hubble-residual dispersion is significantly reduced by avoiding this bimodality. We discuss possible strategies for mitigating this bias in Sect. 6.3.

6.1. Evolution of the SNe Ia Magnitude with Redshift

6.1.1. Evolution Model

The mean sSFR is known to increase with redshift (e.g. Pérez-González et al. 2008), which most likely decreases the proportion of SNe associated with locally passive environments (Sullivan et al. 2006; Hopkins & Beacom 2006). Because of the \(H_{\alpha}\) bias, the average SN brightness is expected to be redshift dependent.

We define \(\psi(z)\) as the fraction of SNe located in locally passive environments (Iae) as a function of redshift. Assuming that the brightness offset between Ia\(\alpha\) and Iae is constant with redshift, the mean corrected B-magnitude of SNe Ia at maximum light can then be written as:

\[
\langle M_{B}^{\text{corr}} \rangle(z) = (1 - \psi(z)) \times \langle M_{B}^{\text{corr}} \rangle_{\text{Ia}\alpha} + \psi(z) \times \langle M_{B}^{\text{corr}} \rangle_{\text{Iae}} = \langle M_{B}^{\text{corr}} \rangle_{\text{Ia}\alpha} + \psi(z) \times \delta(M_{B}^{\text{corr}})(\text{Iae - Ia}\alpha).
\]

(3)

Pérez-González et al. (2008) demonstrate that the global galactic sSFR increases by a factor of \(\sim 40\) between \(z = 0\) and 2 (see also Damen et al. 2009). This evolution can be adequately approximated as:

\[
\log(sSFR)(z) \approx \log(sSFR_{0}) + 0.95 \times z.
\]

(4)

Since sSFR measures the fraction of young stars in a galaxy, we suggest as a toy model that the proportion of SNe from locally passive environments evolves in complement (Sullivan et al. 2006) and therefore decreases with \(z\):

\[
\psi(z) = (K \times 10^{0.95z} + 1)^{-1}.
\]

(5)

By definition of the Ia\(\alpha\)/Iae subgroups, the SNfactory sample sets the normalization to \(\psi(z = 0.05) = 41/82 = 50 \pm 5\%\) (Cameron 2011); hence \(K = 0.90 \pm 0.15\).

Then, using SN, CMB, BAO, \(H_{0}\) constraints as in Suzuki et al. (2012), along with the assumption that the Universe is flat, we estimate the impact of a bias in SN Ia luminosity distance measurements. Relative to existing SN cosmological fits, we find that shifting the SN Ia luminosity distances according Eqs. 3 and 5 would shift the estimate of the dark energy equation of state by \(\Delta w \approx -0.06\) (D. Rubin, private communication, as estimated using the Union machinery, Kowalski et al. 2008; Amanullah et al. 2010; Suzuki et al. 2012).

6.1.2. Prediction of the Mass Step Evolution

The \(H_{\alpha}\) bias is due to a brightness offset between SNe Ia from locally star-forming and locally passive environments. Guided by Fig. 10, in Sect 5.2.2 we then made a connection between the \(H_{\alpha}\) bias and the mass-step by noting the strong change in the proportion of SNe Ia\(\alpha\) and SNe Iae on either side of the canonical mass division at \(\log(M/M_{\odot}) = 10\).

In Appendix A the mathematical connection between the \(H_{\alpha}\) bias and the amplitude of the mass step is laid out. To a good approximation, the near absence of bright SNe Ia\(\alpha\) among low-mass hosts means that the low-mass plateau is equal to the average magnitude of the SNe Iae, and is therefore constant with redshift. By contrast, the brighter high-mass plateau has been shown to arise from a subgroup of bright SNe Iae; thus, the amplitude of the mass-step will evolve along with the fraction of SNe Iae, as given by \(\psi(z)\).

Thus, while local \(H_{\alpha}\) measurements are not available for high-redshift SNe Ia in the literature, our hypothesis – that the redshift evolution of the fraction of SNe Iae given our toy model Eq. 5 induces a reduction of the influence of the bright SNe that create both the mass-step and the \(H_{\alpha}\) bias – can be tested using the same evolutionary form, \(\psi(z)\). We consequently predict (see Appendix A.2) that the amplitude of the mass-step, \(\delta(M_{B}^{\text{corr}})(H - L; z)\), evolves as:

\[
\delta(M_{B}^{\text{corr}})(H - L; z) \approx \psi(z) \times \frac{\delta(M_{B}^{\text{corr}})(H - L; z = 0.05)}{\psi(z = 0.05)},
\]

(6)

where setting the constant term, \(\delta(M_{B}^{\text{corr}})(H - L; z = 0.05)\), equal to our measured mass step provides the normalization.
Fig. 10. Corrected Hubble residuals as a function of the total host stellar mass, showing the mass step. Markers follow the same color and shape code as in Fig. 6. Top: total host stellar mass distribution per \( \Sigma_{\text{host}} \) subgroup. Right: \( \Delta M_{\text{corr}}^B \) distribution per \( \Sigma_{\text{host}} \) subgroup (a) and per mode (b), as shown in Fig. 8. Horizontal red and gray lines indicate \( M_1 \) and \( M_2 \) weighted mean values respectively. Central panel: Left and right green horizontal lines indicate the weighted mean \( \Delta M_{\text{corr}}^B \) of SNe Ia hosted by galaxies more or less massive than \( \log(M/M_\odot) = 10 \) (vertical gray line). The difference between those two magnitudes defines the “mass-step.”

6.1.3. Verification of Mass-Step Evolution

Figure 11 shows the predicted redshift evolution of the amplitude of the mass step assuming our simple SNfactory-normalized model. We compare this model to mass steps measured using literature SNe from SNLS, SDSS and non-SNfactory low-\( z \) datasets (Sullivan et al. 2010; Gupta et al. 2011; Kelly et al. 2010, respectively) from the combined dataset of Childress et al. (2013a). We split those data into four redshift bins with equal numbers of SNe Ia (\( \approx \) 120 SNe Ia in \( z < 0.18, 0.18 < z < 0.31, 0.31 < z < 0.6 \) and \( 0.6 < z \) ranges), and we measure for each bin the magnitude offset between SNe in low- and high-mass hosts for a step located at \( \log(M/M_\odot) = 10 \). Figure 11 shows that our simple model qualitatively reproduces the measured mass step evolution with redshift. Relative to a fixed mass-step anchored by the SNfactory data, our model gives 1.6% evolution with redshift. Relative to a fixed mass-step anchored by the SNfactory data, our model gives \( \Delta \alpha^2 \approx -5.7 \) for the literature data sets. This provides external confirmation of behavior consistent with the \( H_\alpha \) bias at greater than 98% confidence.

6.1.4. Interpretation and Literature Corrections

From this observation we draw several conclusions. (1) The amplitude of the mass step indeed decreases at higher redshift, so host mass cannot be used, as it has been, as a third SN standardization parameter (Lampeitl et al. 2010; Sullivan et al. 2010). (2) The observed mass steps follow the predicted evolution based on the \( H_\alpha \) bias quite well. This in turn lends further support to the idea that the \( H_\alpha \) bias is the origin of the magnitude offset with host mass. As the mass step bias is observed in different data sets, the \( H_\alpha \) bias appears to be a fundamental property of SNe Ia standardized using SALT2. (3) Any ad hoc correction of the mass step by letting SNe Ia from low- and high-mass hosts have different absolute magnitudes will be inappropriate as this assumes that high-mass hosted SNe are brighter in a constant way (Conley et al. 2011), ignoring the observed redshift evolution. Doing so will bias the SN Ia population from high-mass hosts that dominate at higher \( z \), and miss the observed evolution of mean SNe Ia magnitude. Therefore, such a correction will not remove the bias on the dark energy equation of state, which we estimate to be \( \Delta w \sim 0.06 \).

Of course application of a fixed mass-step correction remains useful for bringing into agreement two datasets at the same redshift that have different proportions of low-mass and high-mass host galaxies due to survey selection effects. Whether or not a correction using a fixed mass-step might accidentally help or hurt in correcting the redshift evolution of the \( H_\alpha \) bias depends on the – currently unknown – correlation of the parameters of Eqs. 3 and 5 with the redshift evolution in the ratio of high- to low-mass host galaxies.

6.2. Type Ia SNe: Homogeneous SALT2 Candles

The SNe Ia are unimodal in stretch and in corrected Hubble residuals, and are therefore free from the aforementioned \( H_\alpha \) bias/mass step. The \( \Delta M_{\text{corr}}^B \) distribution for this new group of supernovae, when the SALT2 standardization is performed on this subsample only, is shown in Fig. 12.

Article number, page 13 of 19
SNe Ia standardization generates a smooth symmetric residual distribution, with a significantly smaller magnitude dispersion of $\sigma = 0.105 \pm 0.012$ mag (after 3σ clipping) than the full initial sample ($\sigma = 0.152 \pm 0.011$ mag, no outlier). This dispersion is in agreement with the original $M_1$ fit (0.099 $\pm$ 0.009 mag), and corresponds to a significant reduction of $\sim 30\%$ of the Hubble residual dispersion.

In order to check the robustness of this result we conducted several additional tests. First we considered the effect of including the 3σ outlier, SNF20070701-005. Doing so increases the residual standard deviation to $0.126 \pm 0.014$ mag (nMAD of 0.108 mag), but we note that this outlier falls within the brighter part of the distribution, potentially polluted by $M_2$ SNe; this SN might just be a case of misassociation with a star-forming environment, as discussed in Sect. 3. This possibility is reinforced by the fact that this host is globally passive, having log(sSFR) $= -10.8$ (Childress et al. 2013a).

Next, we performed a permutation test based on independent standardization trials for 41 randomly selected SNe from the full sample. The results attest to the high significance of the environmental selection, giving $p = 1.9 \times 10^{-3}$.

Finally, K-fold cross-validation was employed in order to measure the predictive power of our model. Since it avoids over-fitting the sample, cross-validation results are not expected to be as good as the original fit (Kim et al. 2013). We find $\sigma = 0.117 \pm 0.014$ mag using $k = 10$, compatible with our original results. The quoted error includes a marginal dispersion of 0.004 mag from random “fold” selections.

### 6.3. Mitigation Strategies

The Hα bias is a concern for cosmology, as it reveals a local environmental dependency – most probably a progenitor effect – not accounted for by current SN standardization methods. It is necessary for ongoing and future surveys to consider it. The best solution would be if additional light curve or spectral features could be identified that can be used to remove the impact of local host properties. Another possibility would be to include the bimodality in the cosmology fitter, treating the redshift dependence and relative fraction of passive environments as free parameters. However, this seems perilous as it could mask or induce signatures of exotic dark energy, and likely would require lightcurves with much better statistical accuracy in order to resolve the bimodality. Implementation of our model from Sect. 6.1.1 also could be considered. Examining these and other model-dependent correction possibilities is left for future work. Alternatively, it could prove useful to focus on the Ia$\alpha$ subgroup for cosmological analyses, since these appear to be free of environmental biases.

For cosmological measurements naturally it is not permissible to split the SN Ia sample based solely on Hubble diagram residuals, e.g. one cannot directly select the homogeneous Mode 1 SNe only. However, one may select a subsample of SNe Ia based on their local environment properties: it is then possible to remove the brighter Mode 2 – exclusive to locally passive environments – by discarding the entire Ia$\alpha$ group. This is not as draconian as it may sound; while only $\sim 50\%$ of the sample would be retained, this subset has roughly 1.8x as much statistical weight per SN. Thus, the statistical power is nearly the same as using the full sample. Of course obtaining local environment measurements could be observationally expensive, but Fig. 11 indicates that most of the bias is at lower redshifts, where local environment measurements are less difficult. Since Ia$\alpha$ appear to be dustier, this might add some complications, but in our dataset
the Ia\(\alpha\) standardize well despite this. We note that removing SNe from globally passive hosts will only remove approximately half of the SNe Ia. However, at least then local measurements would not be needed for these.

In conclusion, SNe Ia from passive environments (Ia\(\epsilon\)) appear to cause the known (yet not understood) environmental biases, and we raise the possibility of removing them for cosmological studies. As SNe Ia\(\epsilon\) form an homogeneous subgroup of standardizable candles, free from environmental biases and therefore showing a tighter dispersion on the Hubble diagram, they could be used exclusively for cosmological analyses.

### 7. Robustness of the Analysis

In this section, we analyze the robustness of our results, by testing potential issues in our analysis: (1) the impact of seeing given our 1 kpc aperture; (2) the influence of SNe potentially misassociated with H\(\alpha\) signal from host galaxy core; (3) the influence of the \(\Sigma_{H\alpha}\) boundary defining the Ia\(\epsilon\) and Ia\(\alpha\) subgroups. The general conclusion of these tests is that our results are not significantly affected by changes in our assumptions.

#### 7.1. Restframe Aperture and Redshift Bias

All our spectra have been averaged over an identical spatial aperture of 1 kpc radius (see Sect. 2.2.3). However, the atmospheric seeing PSF correlates spaxels on the arcsecond scale. For the SNfactory dataset the median seeing is 1:\(\prime\):1. This corresponds to a projected correlation length of \(0.65\) kpc at \(z = 0.03\); \(1.1\) kpc at \(z = 0.05\), and \(1.6\) kpc at \(z = 0.08\). The redshift therefore has an influence on the amount of independent information in the 1 kpc radius aperture around the SN due to the seeing. Seeing also allows contamination of the local environment from bright sources outside the aperture.

However, a Spearman rank correlation analysis shows no correlation between \(\log(\Sigma_{H\alpha})\) and \(z\) (\(r_s = 0.17\), \(p_s = 0.14\)), and both \(\Sigma_{H\alpha}\) subgroups have similar redshift distributions (\(p_{KS} = 0.25\)). Consequently, we believe that our analysis is relative unaffected by a redshift bias induced by seeing.

#### 7.2. SNe with Potentially Misassociated H\(\alpha\) signal

SNe close to the center of very inclined hosts (referred to as “p.m.s.”, see Sect. 3) have been directly removed from the main analysis, given the possible misassociation with H\(\alpha\) from the core of the galaxy. However, when we include those SNe, none of the previous results are significantly impacted:

- **Color Relation:** The observed correlation between \(c\) and \(\log(\Sigma_{H\alpha})\) is slightly more significant, with a Spearman rank correlation coefficient of \(r_s = 0.22\) (\(p_s = 0.035\));
- **H\(\alpha\) bias:** The bias increases marginally, with \(\delta(M_{B,corr}(Ia\epsilon - Ia\alpha)) = -0.102 \pm 0.031\) mag (\(p_{KS} = 6.5 \times 10^{-3}\));
- **Stretch and host mass:** \(x_1\) and the total host stellar mass remain uncorrelated for SNe Ia\(\epsilon\) (\(r_s = 0.07\), \(p_s = 0.66\));
- **SNe Ia\(\epsilon\) dispersion:** The Ia\(\alpha\) \(\Delta M_{B,corr}\) dispersion increases to \(0.115 \pm 0.012\) mag (\(p = 0.011\)), which is still compatible with our fiducial result.

#### 7.3. Influence of the Ia\(\alpha\)/Ia\(\epsilon\) Boundary

In our fiducial analysis the division between locally passive (Ia\(\epsilon\)) and locally star-forming (Ia\(\alpha\)) subgroups was set at the median value \(\log(\Sigma_{H\alpha}) = 38.35\) of a 82 SN sample. The confidence interval for this population split is 37–45 (Cameron 2011), and we now demonstrate the robustness of our analysis to these Ia\(\alpha\)/Ia\(\epsilon\) limit shifts.

**H\(\alpha\) bias:** The bias changes within the errors bars, with \(\delta(M_{B,corr}(Ia\epsilon - Ia\alpha)) = -0.101 \pm 0.031\) mag and \(\delta(M_{B,corr}(Ia\alpha - Ia\epsilon)) = -0.075 \pm 0.032\) mag for 37 and 45 Ia\(\epsilon\), respectively.

Stretch and host mass: \(x_1\) and the total host stellar mass of the SNe Ia\(\epsilon\) remain uncorrelated in both cases, giving \(p_s = 0.84\);

SNe Ia\(\epsilon\) dispersion: The Ia\(\alpha\) \(\Delta M_{B,corr}\) dispersion is the same within the error bars, with \(0.115 \pm 0.012\) mag and \(0.112 \pm 0.012\) mag for 37 and 45 Ia\(\epsilon\), respectively.

Further, in Sect. 3 we pointed out cases of SNe Ia\(\epsilon\) in globally star-forming hosts located near our division point, e.g., having \(\log(\Sigma_{H\alpha}) \sim 38\) and SFR \(> -10\). Whether or not they truly are locally passive or locally star-forming is therefore somewhat uncertain. Here we show that our main results do not depend on whether or not those SNe are included in the Ia\(\epsilon\) subgroup.

However, three of these cases are bright and have been counted as \(M_2\) in our fiducial analysis, therefore moving them from Ia\(\epsilon\) to Ia\(\alpha\) increases the dispersion of Hubble residuals of the SNe Ia\(\epsilon\) subset.

**H\(\alpha\) bias:** The bias marginally changes, with \(\delta(M_{B,corr}(Ia\epsilon - Ia\alpha)) = -0.097 \pm 0.032\) mag.

Stretch and host mass: \(x_1\) and the total host stellar mass of the SNe Ia\(\epsilon\) remain uncorrelated, giving \(p_s = 0.57\);

SNe Ia\(\epsilon\) dispersion: The Ia\(\alpha\) \(\Delta M_{B,corr}\) dispersion is degraded by the inclusion of bright SNe that skew the normal distribution: \(\sigma = 0.144 \pm 0.014\) mag (no SNe have been clipped).

### 8. Summary & Conclusion

Using the SuperNova Integral Field Spectrograph (SNIFS), we have assembled a sample of 89 nearby SNe Ia in the redshift range \(0.03 < z < 0.08\) with accurate measurements of the H\(\alpha\) surface brightness within a 1 kpc radius (\(\Sigma_{H\alpha}\)) used as a tracer of young stars in the SN neighborhood.

This sample has been split in two at the median value \(\log(\Sigma_{H\alpha}) = 38.35\), which happens to correspond to the mean warm interstellar medium H\(\alpha\) surface brightness of galaxies (Oey et al. 2007) and to the mean H\(\alpha\) sensitivity level at our highest redshift. SNe with low \(\Sigma_{H\alpha}\) have then been referred to as “locally passive” (Ia\(\epsilon\)) while those with high \(\Sigma_{H\alpha}\) are designated as “locally star-forming” (Ia\(\alpha\)). The wide range of measured \(\Sigma_{H\alpha}\), indirectly confirms the existence of SNe Ia\(\epsilon\) associated to both young and old stellar populations. We have then studied variations of SNe properties as a function of this local host parameter.

**Color:** Our local analysis highlights a 2\(\sigma\) significance correlation between \(\log(\Sigma_{H\alpha})\) and the SALT2 color \(c\), with the SNe Ia\(\epsilon\) being redder, as expected (Charlot & Fall 2000).

**Stretch:** The relationship between SN light-curve stretch and local star formation activity is more complex than that suggested by previous global host studies. Faster declining SNe (\(x_1 < -1\)) are indeed strongly favored by locally passive environments, but passive local environments also host SNe with moderate stretches. Lower stretch SNe Ia are hosted in locally passive environments, but we find that moderate stretch SNe Ia are hosted by all types of environments. The local perspective also shows...
that the correlation between the host stellar mass and SN stretch is entirely created by the SNe Ia. The stretches of SNe Ia, from locally star-forming regions are uncorrelated with the total stellar masses of their hosts.

Hubble residuals: After routine SALT2 standardization using stretch and color, we have shown that the SN Ia Hubble residuals ($\Delta M_{\text{corr}}$) are significantly environment-dependent. SNe Ia from locally passive regions are 0.094 ± 0.031 mag brighter than SNe Ia from locally star-forming regions. This $H_\alpha$ bias originates from a bimodal structure in the Hubble residual distribution. The first mode, denoted as $M_1$, is present in all environments, independent of the local star formation activity. The second mode, $M_2$, is intrinsically brighter and exclusive to locally passive environments, and predominantly occurs in high-mass hosts. We noted that this peculiar structure naturally explains the previously observed “mass step”, i.e. the offset in brightness between SNe from low- and high-mass hosts (e.g. Childress et al. 2013a). This suggests that the $H_\alpha$ bias is not exclusive to our sample, and is of a more fundamental origin than the global host effect. Additional SN data, with measurement uncertainties below the 0.1 mag, will be critical for confirming the Hubble residual bimodality. Our analysis does not suggest any significant dependence on the local $H_\alpha$ environment of the stretch or color coefficients used in standardization.

Cosmological implications: The $H_\alpha$ bias is a concern for cosmology since the fraction of SNe in star-forming environments most likely changes with redshift, which implies an evolution with $z$ of the mean $B$-magnitude of SNe Ia after standardization. Using a simple toy model based on the evolution of the specific star formation rate of galaxies with redshift, we estimated this effect could shift the measurement of the dark energy equation of state parameter by $\Delta w \sim -0.06$. Currently-employed constant mass-step corrections might accidentally reduce or increase the bias on $w$, but do not remove it. Moreover, the amplitude of the mass step is shown to evolve with redshift as predicted, which supports our claim that both the $H_\alpha$ bias and the mass-step arise from the same underlying phenomenon. Future cosmological analyses will need to consider these environmental dependencies. An ideal solution would be to find additional light curve or spectral features able to correct this bias. Another solution would be to focus on a subsample of SNe Ia free from this known – yet not understood – biases.

SNe Ia as homogeneous SALT2 candles: SNe Ia from locally passive environments (Iae) appear to be the cause of all the biases we have observed. We have raised the idea of removing them from cosmological fits for this reason. The remaining bias-free SNe Ia have an intrinsic Hubble residual dispersion reduced to 0.105 ± 0.012 mag, suggesting that a selection on local environment would significantly improve the quality of SNe Ia as cosmological distance indicators. We further noted that this remaining dispersion is entirely consistent with our measurement uncertainties; no intrinsic dispersion is necessary. The trade-off would be minor loss in net statistical power compared to using the full SN sample and the need for measurements of the local environment, versus a far more serious bias.

At this juncture SN cosmology is limited by systematic errors. (Conley et al. 2011; Saunders et al. 2013). Calibration issues are thought to set the current limits, but our first analysis of the local SN environments has revealed strong correlations between SNe and the star-forming activity of their immediate environment. This is most likely caused by our limited knowledge of the progenitors of the SNe Ia, the existence of potential SN subgroups, and the evolution with redshift of these standardizable candles.

For future SN cosmology efforts we thus suggest further studies exploring the properties of SN Ia local host environments. Notably, the following local host properties may bring essential clues leading to the minimization of progenitor dependencies: gas and stellar metallicities; star formation history surrounding the SNe, and local interstellar dust extinction. Continuing to refine these measurements will constitute a major step forward in the direction of constructing an accurate “likes-to-likes” SN cosmology.

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Article number, page 16 of 19
Appendix A: Relation between the H\(_\alpha\) bias and the Mass Step

In this Appendix we provide the mathematical details needed to understand the relation between the \(\Sigma_{H\alpha}\) group magnitudes and the observed mass step. This is all that is needed to understand the relation between the numerical values of the H\(_\alpha\) bias and the mass step in the SNfactory dataset.

To begin, the dataset is partitioned into four subsets consisting of SNe Ia\(_\alpha\) and SNe Ia\(\epsilon\) above and below the canonical mass division point of log(M/M\(_\odot\)) = 10. We denote the number in each subset as \(N_{a,l}\), \(N_{a,h}\), \(N_{\epsilon,l}\), and \(N_{\epsilon,h}\), with \(L\) and \(H\) symbolizing SNe Ia in low- and high-mass hosts, respectively. Likewise, the mean Hubble residuals for each subset are denoted as \(\langle \Delta M_{B}^{\text{corr}} \rangle_{a,l}\), \(\langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}\), \(\langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l}\), and \(\langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h}\).

In order to make the equations more readable we introduce the following notation for fractions: \(F_{X}\) means "the fraction of SNe from subset \(X\) that have property \(Y\)." For instance \(F_{H}^{L}\) means "the fraction of SNe Ia from high-mass hosts that are Ia\(\epsilon\)". Mathematically, \(B\) is the numerator and \(A\) is the denominator. Naturally, the partitioning imposes the requirement that \(F_{B}^{L} + F_{B}^{H} = 1\), e.g., \(F_{H}^{L} + F_{\epsilon}^{H} = (N_{\epsilon,h} + N_{\epsilon,l})/N_{H} = 1\).

### Appendix A.1: General equations

The H\(_\alpha\) bias, \(\delta(M_{B}^{\text{corr}})_{\text{Ia}\epsilon - \text{Ia}\alpha}\), is defined as the weighted mean difference of the \(\Delta M_{B}^{\text{corr}}\) between the Ia\(\epsilon\) and Ia\(\alpha\) subsamples.

\[
\delta(M_{B}^{\text{corr}})_{\text{Ia}\epsilon - \text{Ia}\alpha} \equiv \langle \Delta M_{B}^{\text{corr}} \rangle_{\text{Ia}\epsilon} - \langle \Delta M_{B}^{\text{corr}} \rangle_{\text{Ia}\alpha}
\]  

(A.1)

The mass-step, \(\delta(M_{B}^{\text{corr}})(H - L)\), is defined as the weighted mean difference of the \(\Delta M_{B}^{\text{corr}}\) between SNe Ia in low-mass and the high-mass hosts.

\[
\delta(M_{B}^{\text{corr}})(H - L) \equiv \langle \Delta M_{B}^{\text{corr}} \rangle_{H} - \langle \Delta M_{B}^{\text{corr}} \rangle_{L}
\]

(A.2)

The individual weighted mean magnitudes entering Eqs. A.1 and A.2 can be written in terms of the weighted mean magnitudes for each portion. Introduction of our \(F_{X}\) notation then gives

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} = \frac{N_{a,l} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + N_{a,h} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}}{N_{a,l} + N_{a,h}} = F_{L}^{a} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{a} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}
\]

(A.3)

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} = \frac{N_{a,l} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + N_{a,h} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}}{N_{a,l} + N_{a,h}} = F_{L}^{a} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{a} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}
\]

(A.4)

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h} = \frac{N_{\epsilon,l} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} + N_{\epsilon,h} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h}}{N_{\epsilon,l} + N_{\epsilon,h}} = F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h}
\]

(A.5)

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} = \frac{N_{\epsilon,l} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} + N_{\epsilon,h} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h}}{N_{\epsilon,l} + N_{\epsilon,h}} = F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h}
\]

(A.6)

Combining these we obtain the equations for the H\(_\alpha\) bias and mass step in terms of the partitioned data:

\[
\delta(M_{B}^{\text{corr}})_{\text{Ia}\epsilon - \text{Ia}\alpha} = F_{H}^{L} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} - F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} - F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}
\]

(A.7)

\[
\delta(M_{B}^{\text{corr}})(H - L) = F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} - F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} - F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}
\]

(A.8)

With this development it is now possible to write the mass step directly in terms of the H\(_\alpha\) bias, as follows:

\[
\delta(M_{B}^{\text{corr}})(H - L) = \delta(M_{B}^{\text{corr}})_{\text{Ia}\epsilon - \text{Ia}\alpha} \times \frac{F_{H}^{L} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} - F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} - F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}}{F_{H}^{L} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} + F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} - F_{L}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} - F_{H}^{\epsilon} \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h}}
\]

(A.9)

Note that in this expression we have simply rearranged terms in order to demonstrate that the same weighted mean magnitudes, just having different signs and fractions, appear in both the numerator and denominator.

### Appendix A.2: Observational constraints

Eq. A.9 is exact when the all of the quantities can be directly measured, as they are in our dataset. But, the variables can be generalized to any similar dataset. In order to be exact, though, local environment observations would be required. However, in the main text we presented two observational constraints that can be used to greatly simplify Eq. A.9. First, we have shown in Sect. 5.2.2 that the averaged \(\Delta M_{B}^{\text{corr}}\) of SNe Ia\(\alpha\) does not depend on the masses of their hosts:

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{a,l} \approx \langle \Delta M_{B}^{\text{corr}} \rangle_{a,h} \approx \langle \Delta M_{B}^{\text{corr}} \rangle_{\text{Ia}\alpha}.
\]

(A.10)

Second, we observed in Fig. 10 that SNe Ia\(\alpha\) and Ia\(\epsilon\) from low-mass hosts share the same mean magnitude (within error bars):

\[
\langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,l} \approx \langle \Delta M_{B}^{\text{corr}} \rangle_{\epsilon,h} \approx \langle \Delta M_{B}^{\text{corr}} \rangle_{\text{Ia}\epsilon}.
\]

(A.11)

Article number, page 18 of 19
As a consequence of these two observations, the right hand side of Eq. A.7 becomes:

\[
F^e_H \langle \Delta M^\text{corr}_B \rangle_{e,H} + F^e_L \langle \Delta M^\text{corr}_B \rangle_{e,L} - (F^e_L \langle \Delta M^\text{corr}_B \rangle_{a,L} + F^e_H \langle \Delta M^\text{corr}_B \rangle_{a,H}) \approx F^e_H \langle \Delta M^\text{corr}_B \rangle_{e,H} + (1 - F^e_H) \langle \Delta M^\text{corr}_B \rangle_{Ia} - \langle \Delta M^\text{corr}_B \rangle_{Ia}
\]

\[
\approx F^e_H \times (\langle \Delta M^\text{corr}_B \rangle_{e,H} - \langle \Delta M^\text{corr}_B \rangle_{Ia}).
\]  

(A.12)

Similarly, the right hand side of Eq. A.8 becomes:

\[
F^H_e \langle \Delta M^\text{corr}_B \rangle_{e,H} + F^H_L \langle \Delta M^\text{corr}_B \rangle_{e,L} - (F^L_e \langle \Delta M^\text{corr}_B \rangle_{a,L} + F^H_L \langle \Delta M^\text{corr}_B \rangle_{a,H}) \approx F^H_e \langle \Delta M^\text{corr}_B \rangle_{e,H} + (1 - F^H_e) \langle \Delta M^\text{corr}_B \rangle_{Ia} - \langle \Delta M^\text{corr}_B \rangle_{Ia}
\]

\[
\approx F^H_e \times (\langle \Delta M^\text{corr}_B \rangle_{e,H} - \langle \Delta M^\text{corr}_B \rangle_{Ia}).
\]  

(A.13)

Finally, using the relation\( F_e^H / F^e_H = \left( N_{e,H} / N_H \right) \times \left( N_e / N_{e,H} \right) = \left( N_e / N \right) \times \left( N / N_H \right) = F_e / F_H \), where \( F_e \) is the fraction of SNe Ia, and \( F_H \) the fraction of SNe Ia from high-mass hosts, Eq. A.9 can simply be expressed as:

\[
\delta \langle \Delta M^\text{corr}_B \rangle_{Ia} \approx F_e \times \delta \langle \Delta M^\text{corr}_B \rangle_{Ia} - \langle \Delta M^\text{corr}_B \rangle_{Ia}
\]  

(A.14)

In the main text, the dependence of \( F_e \) with redshift is denoted \( \psi(z) \), and \( \delta \langle \Delta M^\text{corr}_B \rangle_{Ia} \) is assumed to be constant. Furthermore, based on the dataset we complied in Childress et al. (2013a), \( F_H \) appears to be constant within 10% up to \( z \sim 1 \). Subject to these approximations, we conclude that the mass-step evolution is simply proportional to \( \psi(z) \), as given in Eq. 6.