Artificial Neural Network Based SIW Bandpass Filter Design Using Complementary Split Ring Resonators

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Abstract—A novel Artificial Neural Network (ANN) based two Substrate integrated waveguide (SIW) bandpass filters comprising Complementary Split Ring Resonators (CSRRs) are proposed in this paper. These CSRRs are modelled on the upper layer of the SIW cavity. A feed forward multilayer perceptron (FF-MLP) neural network is used to optimize the physical dimensions of the proposed filters. To validate the analytical results, physical prototypes of the proposed filters are fabricated, and a measurement is carried out with a Combinational Network Analyzer (Anritsu-MS2037C), and the obtained experimental results agree well with the estimated results using full wave analysis. Within the passband from 8.22 to 8.95 GHz, $S_{12}$ of the first filter shows better than $-0.5$ dB insertion loss (IL) and a fractional bandwidth of 8.5%, and within the passband from 8.21 to 8.73 GHz, the second filter shows IL about $-0.8$ dB and a fractional bandwidth of 6.1%.

1. INTRODUCTION

Substrate Integrated Waveguide (SIW) filters have recently attracted a lot of attention because of their high efficiency, easy fabrication process with simple printed circuit board (PCB) technology, small size, low insertion loss, high selectivity, and ease of integration with microwave and millimetre wave circuits [1, 2]. In modern communication systems, one of the important requirements is miniaturization. SIW bandpass filter has been designed and investigated using slow wave method [3, 4]. SIW structures are typically composed of conducting vias which are placed in a dielectric substrate that connects two parallel metal plates, enabling the use of traditional rectangular waveguide components in planar form. The conventional PCB technique can be used in SIW based passive, active devices, microwave components, and antennas. The latest developments in SIW technology in terms of its modelling, design, and technological implementation of SIW structures and components have been reported [5–8].

To acquire compact size and modular geometry, a new type of quasi-elliptic pass-band filters based on mushroom-shaped metallic resonators in SIW technology has been proposed [9]. SIW bandpass filter with a cross-shaped cavity that realizes six symmetrically simulated modes out of first eight higher order resonant modes has been proposed [10]. An SIW band-pass filter having wide and sharp stop band, which differs from filters with a direct coupling between input and output has been proposed [11]. An SIW bandpass filter, modelled on a double layer dielectric substrate consisting of metallic via holes in order to realize the classical H-plane filter has been proposed [12]. Two cascaded mushroom resonators have been modelled on the SIW cavity that works as a dual band bandpass filter has been presented [13]. On the waveguide top metal layer, a number of cross-slot patterns have been modelled to act as dual mode SIW filters [14].

The performance of SIW filters can be improved by using some special types of electromagnetic topologies like split ring resonator (SRR) and complementary split ring resonator (CSRR) and have been
adapted into SIW technology [15]. A novel diamond-shaped CSRR has been proposed and investigated based on an SIW bandpass filter [16]. An extended doublet bandpass filter that uses an SIW cavity with CSRRs on the top layer has been proposed, and a single layer bandpass filter with two transmission zeros (TZ) was analyzed [17]. An SIW filter with square CSRRs has been proposed, and the characteristics of passband have been observed by varying the directions of the CSRRs [18]. CSRR has been modelled on the top surface of the SIW that provides a passband below the initial cutoff frequency of the waveguide TE_{10} mode [19]. By loading CSRRs onto the SIW cavity, the SIW bandpass filters have been achieved in compact size and high selectivity [20]. A double sided CSRR half mode SIW filter that provides lower resonant frequency than the conventional model because of the coupling effect between CSRRs of the upper and lower plates has been proposed [21]. Based on evanescent-mode propagation, a compact SIW bandpass filter using broad side coupled CSRR [22] and fractal open complementary split-ring resonators (FOCSRRs) unit-cell has been presented [23]. Complementary open-ring resonators (CORRs) loaded half mode substrate integrated waveguide (HMSIW), with many transmission zeros and wide stopband, have been proposed [24]. Novel dual mode SIW filters that can provide multiple transmission zeros have been proposed [25].

One of the issues with designing SIW components and RF circuits in the above literature is that the simulation actually needs a lot of calculations, so optimization of the parameters takes a very long time. ANN has been chosen as an alternative method to design microwave circuits and devices, hence ANNs have been used to design circular and rectangular resonators modelled in SIW technology [26, 27]. A back-propagation neural network-based approach for modelling the SIW power dividers has been proposed [28]. In order to model and optimize the microwave components and devices, an efficient hybrid sampling method has been proposed to get optimum design parameters by using the ANN model [29].

The main contribution of the proposed research work is a feed forward multilayer perceptron (FF-MLP) neural network that has been used to optimize the proposed filter parameters. In this work, two networks with 2 x 12 x 1 and 1 x 8 x 1 have been used. The trainlm function in MATLAB has been used to efficiently train the FF-MLP neural networks. The $S_{11}$ parameter has been calculated to evaluate the proposed networks, and the results obtained are in good agreement with the simulated results. Instead of a single CSRR, two CSRRs have been employed to enhance the proposed band pass filter’s roll-off rate.

This paper is organized as follows. Section 2 explains how the basic topology of the proposed SIW filter is designed. Section 3 explains how the filter parameters are optimized using neural networks. Section 4 shows how the filter was simulated and the simulation results. Section 5 provides the fabrication process, measurement setup, and the measured results plotted against the simulated ones.

2. DESIGN OF CROSS SHAPED SIW CAVITY WITH CSRR

The proposed cross shaped SIW cavity topology is depicted in Figure 1. The basic SIW topology consists of three layers. The perfect electric conductor (PEC) is used as bottom layer and top layer, and the middle layer is dielectric material. The dielectric material used is Rogers RO4003C with dielectric constant $\varepsilon_r = 3.55$ and height of the substrate $h = 0.81 \text{ mm}$. The optimized design dimensions of this SIW cavity are as follows. The length of the SIW cavity is $L = 40.8 \text{ mm}$; the length of the dielectric substrate used is $L_{\text{sub}} = 60 \text{ mm}$; the feeding slot length $L_{\text{slot}} = 5.4 \text{ mm}$; the feeding slot width $W_{\text{gap}} = 1.4 \text{ mm}$; the width of the microstrip line is $W_{\text{mst}} = 2 \text{ mm}$; the diameter of the metallic post or via-hole is $d = 1.2 \text{ mm}$. These metallic posts are placed with two different allowable separation distances or pitches (via-to-via distance) of the vias $p = 1.7 \text{ mm}$ and $p_1 = 2 \text{ mm}$. The geometries of this cross shaped SIW cavity in horizontal and vertical directions are the same.

2.1. Design of CSRR

The square shape CSRR is used in the filter design process, and the physical appearance of this CSRR is as depicted in Figure 2. The CSRR acts as an electric dipole, and this CSRR structure is etched on the upper PEC of the SIW cavity. The exited mode of the CSRR is the same as the dominant mode TE_{10} of the SIW cavity.
Figure 1. Cross shaped SIW cavity.

Figure 2. Structure of CSRR.

The CSRR structure resembles an LC resonant circuit. The resonance frequency of the CSRR is computed by the self inductance $L$ and capacitance per unit length $C'$. The resonant frequency of square shaped CSRR is given by [16]

$$f_r = \frac{1}{2\pi\sqrt{L_0C_0}}$$  \hspace{1cm} (1)

where $L_0$ and $C_0$ represent the equivalent inductance and equivalent capacitance of the CSRR structure. The equivalent capacitance $C_0$ can be derived by using the following expression,

$$C_0 = (C_s + C_g)/2$$  \hspace{1cm} (2)

where $C_s$ and $C_g$ are series and gap capacitances of CSRR, and these two capacitances can be found by using some of the SIW filter parameters like width ($w$), metal thickness ($mt$), and free space permittivity ($\varepsilon_0$). In this paper, by using these square shaped CSRRs two SIW bandpass filters are designed.
2.2. SIW Bandpass Filter with Single CSRR

Initially an SIW bandpass filter with single CSRR is designed and fabricated. This design process is done by using SIW crosses shaped topology with the optimized values which have already been mentioned earlier, and then CSRR is loaded into it. The CSRR is etched on the top layer of the structure which is a conducting material (PEC), with the optimized geometrical parameters as follows, \( S_r = 2.8 \, \text{mm}, \) \( S_{r1} = 3.8 \, \text{mm}, \) \( g = 0.4 \, \text{mm}, \) \( g_{in} = 0.4 \, \text{mm}, \) and this total topology is as shown in Figure 3 which is designed and simulated using CST microwave studio. The fabricated prototype model is shown in Figure 9(a).

![Figure 3. SIW bandpass filter with single CSRR.](image)

2.3. SIW Bandpass Filter with two CSRRs

Another SIW bandpass filter is designed with two CSRR rings facing each other with a separation distance \( t = 0.6 \, \text{mm}, \) and it was fabricated. The optimized values are: \( d = 1.2 \, \text{mm}, \) \( L_{sub} = 60 \, \text{mm}, \) \( L = 40.8 \, \text{mm}, \) \( L_{slot} = 5.6 \, \text{mm}, \) \( p = 1.7 \, \text{mm}, \) \( p_1 = 2 \, \text{mm}, \) \( W_{inst} = 1.6 \, \text{mm}, \) \( W_{gap} = 1.4 \, \text{mm}. \)

Now in this topology two CSRRs are etched on the upper conducting layer (PEC), with the optimized geometrical parameters as follows, \( S_r = 2.6 \, \text{mm}, \) \( S_{r1} = 3.4 \, \text{mm}, \) \( g = 0.4 \, \text{mm}, \) \( g_{in} = 0.4 \, \text{mm}, \) as shown in Figure 4 and designed and simulated using CST microwave studio, and the fabricated prototype model is shown in Figure 9(b).

3. ANN OPTIMIZATION

3.1. Typical Structure of the Artificial Neural Networks (ANN)

The basic structure of ANN shown in Figure 5 consists of three sections. The first section is the input layer; the second section is hidden layer which has one or more sub-layers; and the third section is the output layer. In each stage, there are some processing units which are known as neurons, and all these neurons are interconnected to each other. Each neuron receives some information from one or more other neurons and is processed further. The neural network produces an output which is a weighted sum of all the information from input layer and hidden layer. There are several types of neural networks, which are categorized based on the neuron types and the interconnections between them.

The input to the neurons in the input layer is externally (out of the neural network) applied. The output of the input layer neurons acts as input to the hidden layer neurons. The information is processed
3.2. Filter Parameters Optimization Using ANN

The physical parameters of the proposed filter are optimised by using ANN in MATLAB. Basically there are many types of neural networks. Among them, FF-MLP neural network is used for the optimization of proposed filter parameters.

3.2.1. Neural Network Training

The $S_{11}$ output data collected from the parametric analysis in CST are used as training data, shown in Table 1 and Table 2. Two neural networks are designed to optimize the filter parameters. The first network contains one input layer with two neurons, one hidden layer with 12 neurons, and one output layer with one neuron. In order to train the first network, the data shown in Table 1 are used. The filter parameters among all these hidden layer neurons, and finally the output of the hidden layer acts as input to the output layer.
parameters $S_r$ and $S_{r1}$ are applied to the input layer, and $S_{11}$ is the target value. The second network also consists of one input layer with single neuron, one hidden layer with 8 neurons, and the output layer with one neuron, and it is trained with the data shown in Table 2. The second network is used to optimize the filter parameter $W_{gap}$. These two neural networks are trained using Levenberg Marquart (LM) algorithm, for which the ‘trainlm’ function is used, and log-sigmoid is used as transformation function. Adaption learning function (LEARNGDM) is used with a learning rate of 0.01.

The training of this neural network is carried out with a learning method known as supervised learning error back propagation method. In this method, the mean square error is back propagated, and the weights are updated accordingly in order to get minimum error. After training the network with the sample data, the weights of this network remain constant, and the neural network is enough trained. Now the neural network is ready to examine with the testing data.

### 3.2.2. Neural Network Testing

After enough training, the neural network is ready for testing with the data shown in Table 3 and Table 4, and the final results are also included in the same table. The testing data and the $S_{11}$ obtained in CST MWS agree well with each other with minimum mean square error.
Table 3. Testing data for first network.

| S. No. | $S_r$ (mm) | $S_{r1}$ (mm) | $S_{11}$ (dB) (CST) | $S_{11}$ (dB) (ANN) |
|--------|------------|---------------|----------------------|---------------------|
| 1      | 2.0        | 3.0           | -6.441               | -6.5070             |
| 2      | 2.1        | 3.1           | -10.646              | -10.5359            |
| 3      | 2.2        | 3.2           | -11.057              | -10.8425            |
| 4      | 2.3        | 3.3           | -11.435              | -11.2598            |
| 5      | 2.4        | 3.4           | -12.89               | -12.9872            |
| 6      | 2.5        | 3.5           | -13.226              | -13.3160            |
| 7      | 2.6        | 3.6           | -14.618              | -14.7271            |
| 8      | 2.7        | 3.7           | -18.247              | -18.3683            |
| 9      | 2.8        | 3.8           | -24.095              | -23.9871            |
| 10     | 2.9        | 3.9           | -23.851              | -23.8316            |
| 11     | 3.0        | 4.0           | -23.359              | -22.7611            |
| 12     | 3.1        | 4.1           | -21.844              | -21.9474            |

Table 4. Testing data for second network.

| S. No. | $W_{gap}$ (mm) | $S_{11}$ (dB) (CST) | $S_{11}$ (dB) (ANN) |
|--------|----------------|----------------------|---------------------|
| 1      | 0.8            | -12.515              | -12.6186            |
| 2      | 0.9            | -13.997              | -13.7384            |
| 3      | 1.0            | -15.505              | -15.5065            |
| 4      | 1.1            | -17.054              | -17.0542            |
| 5      | 1.2            | -18.975              | -18.4913            |
| 6      | 1.3            | -20.912              | -20.9320            |
| 7      | 1.4            | -23.782              | -23.7203            |
| 8      | 1.5            | -23.125              | -23.5102            |
| 9      | 1.6            | -22.344              | -22.3218            |

4. RESULTS AND DISCUSSION

The simulated results are as shown in Figure 6. Figure 6(a) shows the transmission characteristics of the SIW cavity filter with single CSRR slot, which was designed and simulated using CST microwave studio. From the graph it is clear that there are two closely spaced resonances observed at 8.4 GHz and 8.6 GHz, with the passband centre frequency of 8.5 GHz. Significantly one of the resonant frequencies is caused by the CSRR, and the other resonant frequency is because of the SIW cavity. The proposed filter offers a good reflection which is better than $-10$ dB, and the reflection bandwidth is 485 MHz, from 8.29 to 8.77 GHz. The transmission bandwidth at $-1$ dB is 480 MHz, and it is between 8.3 GHz and 8.78 GHz. At $-3$ dB, the transmission bandwidth is 730 MHz, and it is from 8.22 GHz to 8.95 GHz. Within the frequency range from 8.38 to 8.64 GHz, the return loss is smaller than $-24$ dB.

Figure 6(b) presents the transmission characteristics of proposed SIW band pass filter with two CSRR slots. At $-1$ dB, the bandwidth obtained is 410 MHz, ranging from 8.27 to 8.68 GHz, and the bandwidth considered at $-3$ dB is 530 MHz, which is from 8.21 to 8.73 GHz, with the centre frequency of 8.5 GHz. This filter also shows two resonant frequencies, one at 8.38 GHz and the other at 8.62 GHz. At $-10$ dB, the reflection bandwidth is 460 MHz, from 8.26 to 8.72 GHz. Two proposed filters show an insertion loss about $-0.5$ dB and $-0.8$ dB within the passband region. These filters show high out of band rejection in lower and higher frequency ranges. The first filter shows a transmission zero at
Figure 6. (a) $S_{11}$ and $S_{12}$ of filter with single CSRR. (b) $S_{11}$ and $S_{12}$ of filter with two CSRR.

Figure 7. (a) Parametric response w.r.t $S_r$ and $S_{r1}$. (b) Parametric response w.r.t $W_{gap}$. (c) & (d) Parametric response w.r.t $L$ for both the filters.
7.85 GHz which is introduced by single CSRR slot, and the second filter shows two transmission zeros at 7.73 GHz and 8.8 GHz, because of two CSRR slots. In order to increase the roll-off rate of the band pass filter, two CSRRs have been used instead of single CSRR.

4.1. Parametric Analysis

A set of training data required to train the neural network is generated from the parametric analysis of both the filters, and the corresponding parametric plots are depicted in Figure 7. This analysis was carried out by changing different parameters of these filters like $S_r$, $S_{r1}$, $W_{gap}$, and $L$.

4.2. E-Field Distribution

Figures 8(a) and 8(b) show the electric field distribution of filters with single CSRR and two CSRRs, respectively. The electric field strength of the proposed filters is indicated by the vertical colour ramps (right side of Figures 8(a) and 8(b)). The red colour shifts on the upper surface of the filters represent the growth of the electric field strength. The proposed CSRRs incorporated SIW filters show the TE$_{10}$ (dominant mode) behaviour like conventional rectangular waveguide.

![Electric field distribution](image)

**Figure 8.** (a) Electric field distribution of filter with single CSRR. (b) Electric field distribution of filter with two CSRRs.

5. FABRICATION AND PRACTICAL VALIDATION

The proposed filters are fabricated, and the top views of the two prototype models are shown in Figures 9(a)–9(b), and the back view is shown in Figure 9(c) with dimensions mentioned above. Rogers RO4003C is used as the dielectric substrate with a relative permittivity of $\varepsilon_r = 3.55$ and loss tangent of $\tan \delta = 0.0027$, and the height of the substrate is $h = 0.81$ mm. The fabrication was done by using the standard PCB process. At the initial stage of fabrication, copper metal is used to coat either side of the substrate material. Vias are drilled in order to form the SIW structure, and these vias are coated with copper metal. In the final stage of fabrication, the CSRR slots are etched on the upper PEC as shown in Figure 9. The measurement of prototype models is carried out with the help of Combinational Analyzer (Anritsu-MS2037C), and the measurement setup is shown in Figure 10.

The measured results are compared with the simulated ones as shown in Figure 11, and they are in good agreement. From Figure 11(a) and Figure 11(b), at $-10$ dB it is observed that the measured $S_{11}$ is shifted by 50 MHz (from 8.28 to 8.33 GHz) and 70 MHz (from 8.26 to 8.33 GHz) respectively from simulated $S_{11}$, and at the centre frequency (8.5 GHz), measured $S_{12}$ is shifted by 0.41 dB and 1 dB respectively from the simulated $S_{12}$. The slight mismatch in results is due to the fabrication tolerances, and this deviation is also because SMA connecters are not taken into account while the simulation is...
Figure 9. Fabrication models of SIW BPF. (a) With single CSRR. (b) With two CSRRs. (c) Back view.

Figure 10. Measurement setup.
Figure 11. Simulated and measured results of (a) BPF with single CSRR, (b) BPF with two CSRRs.

performed. At the passband centre frequency, the two results show better than $-22\,\text{dB}$ and $-18\,\text{dB}$ return losses, respectively.

The performance parameters of the proposed bandpass filters, such as passband center frequency, insertion loss, fractional bandwidth, return loss, dielectric substrate, and type of technique used have been compared with the previous literature and are summarized in Table 5. From Table 5 it is clear that the proposed filters provide better insertion loss, fractional bandwidth, and return loss.

Table 5. Comparison of proposed filters with similar bandpass filters.

| Ref. No. | $f_0$ (GHz) | $IL$ (dB) | FBW (%) | $S_{11}$ (dB) | Substrate ($\varepsilon_r$) | Technique |
|----------|-------------|-----------|---------|--------------|-----------------|-----------|
| [15]     | 3.5         | 1.45      | 6       | $-20$        | Taconic RF-30(3) | CSRR      |
| [19]     | 5           | $\approx 2$ | 3.2     | $-16.6$      | Rogers RT Duroid 5880(2.2) | CSRR      |
| [23]     | 2.4         | 1.25      | 10.5    | $-20$        | Rogers RO4003C(3.55) | FOCSRR    |
| [24]     | 5.8         | 0.9       | 8.5     | $-22$        | Rogers RT Duroid 5880(2.2) | CORR      |
| [25]     | (Measured)  | 15        | 1.7     | $\approx -20$ | Rogers RT Duroid 5880(2.2) | --        |
| This work| Filter I    | 8.5       | 0.5     | 8.5          | Rogers RO4003C(3.55) | CSRR, ANN |
| Filter II|             | 8.5       | 0.8     | 6.1          | Rogers RO4003C(3.55) | CSRR, ANN |

$f_0$ = Pass band center frequency; $IL$ = Insertion Loss; $FBW$ = Fractional bandwidth.

Filter I: SIW bandpass filter with single CSRR
Filter II: SIW bandpass filter with two CSRRs
6. CONCLUSION

Two bandpass filters based on SIW with CSRRs are implemented with the help of an FF-MLP neural network. The neural network is trained properly, and the parameters $S_r$, $S_{r1}$, and $W_{gap}$ are optimized. The prototypes of proposed filter configurations are fabricated using PCB combined with plated through hole technology, and the measured results are in good agreement with the simulated results and neural network optimized results. The measured reflection coefficients for the two filters are $-22$ dB and $-18$ dB, respectively, and the insertion losses are $-1$ dB and $-3$ dB, respectively. The computational time of the neural network is very low compared to the full wave simulations performed with CST microwave studio. The mean square error measured between simulated and neural network results is almost negligible. Hence, the FF-MLP neural network with LM algorithm is one of the best parameter optimization techniques, compared to other commercial software.

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