How Grain Boundaries and Interfacial Electrostatic Interactions Modulate Water Desalination via Nanoporous Hexagonal Boron Nitride

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ABSTRACT: To fulfill the increasing demand for drinking water, researchers are currently exploring nanoporous two-dimensional materials, such as hexagonal boron nitride (hBN), as potential desalination membranes. A prominent, yet unsolved challenge is to understand how such membranes will perform in the presence of defects or surface charge in the membrane material. In this work, we study the effect of grain boundaries (GBs) and interfacial electrostatic interactions on the desalination performance of bicrystalline nanoporous hBN using classical molecular dynamics simulations supported by quantum–mechanical density functional theory (DFT) calculations. We investigate three different nanoporous bicrystalline hBN configurations, with symmetric tilt GBs having misorientation angles of 13.2°, 21.8°, and 32.2°. Using lattice dynamics calculations, we find that grain boundaries alter the areas and shapes of nanopores in bicrystalline hBN, as compared to the monocrystalline hBN. We observe that, although bicrystalline nanoporous hBN with a misorientation angle of 13.2° shows an improved water flow rate by ~30%, it demonstrates reduced Na⁺ ion rejection by ~6%, as compared to monocrystalline hBN. We also uncover the role of the nanopore shape in water desalination, finding that more elongated pores with smaller sizes (in 21.8°- and 32.2°-misoriented bicrystalline hBN) can match water permeation through less elongated pores of slightly larger sizes, with a concomitant ~3–4% decrease in Na⁺ rejection. Simulations also predict that the water flow rate is significantly affected by interfacial electrostatic interactions. Indeed, the water flow rate is the highest when altered partial charges on B and N atoms were determined using DFT calculations, as compared to when no partial charges or bulk partial charges (i.e., charged hBN) were considered. Overall, our work on water/ion transport through nanopores in bicrystalline hBN indicates that the presence of GBs and surface charge can lead, respectively, to a decrease in the ion rejection and water permeation performance of hBN membranes.

INTRODUCTION

Increased population, global warming, and industrialization have all put pressure on the supply of fresh and potable water.1–3 Today, about 15% of the world’s population faces challenges in obtaining drinking water.4,5 Although an abundant amount of water is present on the earth’s surface, only 3% of it is available as potable water.5,6 In contrast, the remaining 97% of water is present as salty water in the oceans and seas.7,8 Consequently, desalination of seawater is a promising solution to satisfy the demand for fresh and potable water, in the near and long-term future. Although numerous methods are available for the desalination of seawater, membrane-based reverse osmosis (RO) is extensively used at both commercial and domestic levels due to its higher energy efficiency.7 The performance of a RO system depends significantly on the filtration membrane employed. Thus, the role played by the membrane material in a RO system is very crucial.7 RO systems traditionally use ceramic and polymeric membranes, which face limitations such as lower strength, water permeability, and service life and higher power requirements and maintenance cost.8 In view of these limitations of conventional membranes, researchers are currently exploring nanoporous two-dimensional (2D) materials such as hexagonal boron nitride (hBN) and graphene as desalination membranes.5,9–12 As opposed to graphene, hBN and molybdenum disulfide (MoS₂) membranes provide opportunities for creating anion- and cation-selective membranes, as boron and nitrogen atoms in hBN and molybdenum and sulfur atoms in MoS₂ are positively and negatively charged.
respectively, and can be used to terminate the nanopores.\textsuperscript{10,13} However, the smaller lateral dimensions of 2D materials obtained using various synthesis techniques pose a challenge in terms of scaling up the process.\textsuperscript{6,11,14,15}

Indeed, for commercial water desalination, large-area 2D materials are required to obtain adequate production rates of potable water. Typically, extended 2D layers are produced by the chemical vapor deposition (CVD) method, which inevitably introduces grain boundaries (GBs) in the material due to temperature gradients in the reactor and multiple nucleation sites on the growth surface.\textsuperscript{16} Although the monocrystalline forms of nanoporous hBN and graphene have extraordinary desalination performance,\textsuperscript{6,17,18} the effect of GBs on water permeability and ionic rejection of such membranes is not known. Nevertheless, it is well known that inadvertently induced GBs in these 2D nanosheets alter their mechanical performance and properties.\textsuperscript{19} Furthermore, quantification of the effect of defects on water/ion transport through single-digit nanopores is a prominent knowledge gap in the field.\textsuperscript{20} Over the years, classical molecular dynamics (MD) simulations and quantum–mechanical density functional theory (DFT) calculations have been used to understand and predict the atomic-level phenomena underlying water permeation through and ion rejection by nanoporous 2D materials.\textsuperscript{6,16,17,21–23} However, so far, simulation studies have considered idealized models of nanoporous hBN and graphene that do not contain GBs in them.

In 2015, Surwade et al.\textsuperscript{9} experimentally analyzed the capabilities of nanoporous graphene as a desalination membrane. In their work, the oxygen plasma etching method was used to create nanopores in single-layer graphene. They concluded that the resulting nanoporous graphene membranes exhibit excellent water permeability and 100% salt rejection. Apart from this experimental study, several modeling studies have been carried out to analyze the desalination performance of nanoporous 2D materials.\textsuperscript{6,21–29} In 2012, Cohen-Tanugi et al.\textsuperscript{6} carried out classical MD simulations and concluded that nanoporous graphene shows extraordinary water permeability, which is many times larger than conventional membranes. They also reported that water permeability depends on the nanopore size, edge functionalization, and applied pressure. Subsequently, Konatham et al.\textsuperscript{24} performed MD simulations to analyze the water desalination performance of graphene membranes and reported that nanopores of $\sim$7.5 Å diameter exhibit effective ion segregation, whereas ions easily passed through nanopores with diameters between $\sim$10.5 and 14.5 Å. These studies uncovered the critical role of the nanopore size in modulating water and ion transport through 2D material membranes. In addition to graphene, other 2D materials have also been examined. Heiranian et al.\textsuperscript{23} performed MD simulations to investigate the desalination performance of single-layer nanoporous MoS$_2$ and predicted that nanopores with molybdenum atoms on their edges showed higher water fluxes ($\sim$70% greater than graphene nanopores). Recently, a review on MoS$_2$-based membranes in water treatment and purification was published, wherein the authors summarized several aspects of MoS$_2$ membranes including surface modification.\textsuperscript{30} In another study, Cao et al.\textsuperscript{22} analyzed the desalination performance of 2D metal–organic framework (MOF) membranes using MD simulations and concluded that 2D MOF membranes lead to 3–6 times higher water permeation than traditional membranes. It was also reported that few-layered MOF membranes exhibit higher water flux than single-layer graphene or MoS$_2$ membranes without any drilling of nanopores due to the inherent pore structure of the material.

Besides the above-mentioned 2D nanosheets, hBN nanosheets have also been investigated as separation membranes by various researchers.\textsuperscript{3,10,12,15,17,18,31–33} Chen et al.\textsuperscript{32} experimentally examined the water transport performance of amine-functionalized nanoporous hBN using a positive pressure setup. They found that the hBN membranes are highly stable in various organic solvents and water and showed high water flux and excellent selectivity in organic and aqueous solvents. In other experimental work, Lei et al.\textsuperscript{38} used a thermal treatment method to synthesize nanoporous hBN and demonstrated its potential to purify contaminated water by absorbing various solvents, dyes, and oils. With respect to modeling studies, Garnier et al.\textsuperscript{17} carried out MD simulations to predict the surface tension profile of water molecules close to mono- and multilayer hBN and graphene nanosheets and to investigate water permeability through nanoporous hBN and graphene. The authors established a correlation between the surface tension profile and the water permeation rate. They further reported that the water surface tension was lower on monolayer hBN as compared to monolayer graphene, which resulted in faster water permeation through monolayer nanoporous hBN due to increased wetting. Gao et al.\textsuperscript{38} employed classical MD simulations to determine the desalination performance of hBN nanosheets and investigated how the shape and size of nanopores in hBN affected salt rejection and water permeation. They also showed that triangular nanopores with nitrogen atoms on the edges of the nanopore exhibited high water permeation rates in the range of 0.132–2.752 kg m$^{-2}$ s$^{-1}$ MPa$^{-1}$, which is several times higher than the water permeation rates through commercial RO membranes (0.011 kg m$^{-2}$ s$^{-1}$ MPa$^{-1}$). Davoy et al.\textsuperscript{15} used MD simulations to predict that the water permeability of nanoporous hBN far exceeded that of polymer-based conventional RO membranes. In fact, it was even higher than that through nanoporous graphene. Other studies focusing on unraveling the role of doping,\textsuperscript{8} nanopore edge functionalization,\textsuperscript{10,31,35} and edge type\textsuperscript{16} in modulating water permeation have also been carried out. Nevertheless, in the above-mentioned studies, the electrical potential produced by nanoporous hBN was not validated with quantum–mechanical DFT calculations, although the charges on B and N atoms were derived using some DFT-based charge partitioning schemes. In fact, in some studies, partial charge values from bulk hBN were used, which may lead to underprediction of the water flux. This aspect is crucial because, as we show, electrostatic interactions play a key role in modulating the performance of nanoporous hBN in desalination applications.

From previous studies, it is evident that monocrystalline nanoporous hBN without any geometrical defects exhibits excellent water permeability,\textsuperscript{17} adsorption ability,\textsuperscript{39} mechanical strength, and structural stability.\textsuperscript{18} Nevertheless, as mentioned before, for water desalination applications, large-area 2D materials are required, which would lead to the presence of grain boundaries (GBs) in the membrane. So far, studies have investigated the water desalination performance of nanoporous monocrystalline hBN and no study has considered the effect of GBs on the desalination performance of bicrystalline hBN. In this work, we investigate the role of GBs in modulating the desalination performance of bicrystalline hBN using classical MD simulations. Because GBs and

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nanopores alter the charge distribution within the hBN nanosheet, thereby affecting electrostatic interactions between hBN and water, we use quantum–mechanical DFT to obtain accurate partial charges on the B and N atoms. We also show that the resulting electrostatic interactions significantly affect the desalination performance of nanoporous bicrystalline hBN. Finally, we conclude that the presence of GBs can adversely affect the desalination performance of nanoporous hBN due to the significant decrease in Na⁺ ion rejection through the membrane.

#### METHODS

**Computational Modeling and Simulation Details.** We used classical MD simulations to study the desalination performance of nanoporous bicrystalline hBN using the open-source Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) package. The simulation system for water desalination is illustrated in Figure 1, in which nanoporous hBN was placed parallel to the x–y plane. We used a simulation box measuring 160 Å in the z-direction and periodic in the x–y directions with a cross-sectional area of \( \sim 31 \times 31 \) Å². The nanoporous hBN sheet was fixed at \( z = 0 \) Å, and rigid graphene pistons were placed at \( z = -75 \) and 18.5 Å. The feed-side region of the simulation box was filled with saline water having 22 Na⁺ ions, 22 Cl⁻ ions, and 2000 water molecules, leading to a salt concentration of 35.7 g L⁻¹, close to the value observed in seawater. The permeate (i.e., pure water) side was filled with 500 water molecules. We verified that the use of a larger number of water molecules on the permeate side did not affect our results. Indeed, the water flow rates through a nanoporous monocrystalline hBN membrane at 50 MPa feed pressure were found to be the same when 500 and 2000 water molecules were present on the permeate side, as shown in Figure S1 in Section S1 of the Supporting Information.

In all of the simulations, the atoms in the nanoporous hBN membrane were allowed to vibrate, except for the ones closest to the periodic boundary. The latter atoms were kept fixed to maintain the hBN sheet at \( z = 0 \) Å by zeroing their momentum. Periodic boundary conditions were implemented along all of the three directions. All simulations were carried out at room temperature (298.15 K) and atmospheric pressure (1 atm) in the lateral, i.e., x–y, direction, using the NPₓᵧₚT ensemble. These conditions were maintained using a Nosé–Hoover thermostat and barostat.

After carrying out energy minimization, the system was equilibrated in the NPₓᵧₚT ensemble for a total time period of 50 ps. A short equilibration phase was chosen so that the ions and/or water molecules do not move to the permeate side. The total energy and temperature were recorded during equilibration and are plotted in Figure S2 in Section S2. It can be deduced from Figure S2a,b that the total energy and temperature converge after 50 ps, indicating that the short equilibration time chosen is sufficient. In all of the simulations, a time step of 1 fs was used. Lennard-Jones (1J) interactions were cut off at a distance of 1.2 nm for water–water and hBN–water interactions. Intra-hBN short-range LJ/Coulombic interactions were not considered. Long-range electrostatic interactions were included using the particle-particle–particle-mesh (PPPM) method. Postequilibration, a uniform pressure \( (P) \) was applied on the feed-side piston along the +z-direction, i.e., the flow direction, whereas atmospheric pressure was implemented on the permeate side piston in the –z-direction, as shown in Figure 1. As explained in the Results and Discussion section, three different feed-side pressures, i.e., 50, 100, and 200 MPa, were used, leading to effective pressure values of 46.87, 96.87, and 196.87 MPa, respectively, which are similar in magnitude to the values considered in previous theoretical studies. The applied pressure was implemented in the form of a uniform force, calculated as \( F = PA/n \), where \( P \) denotes the applied pressure, \( A \) is the piston cross-sectional area, and \( n \) is the number of atoms in the piston.

**Details of the Force Fields Used.** In MD simulations, selection of the force-field parameters is very critical, as the accuracy of the simulation critically depends on them. In this work, a hybrid model (combining the Tersoff potential for hBN, the TIP4P/2005 model for water, and 12-6 LJ plus Coulombic interactions between hBN and water) was used to capture the atomic interactions among different atoms. The Tersoff model with parameters suggested by Albe et al. was used to model the nanoporous monocrystalline and bicrystalline hBN membrane, as done previously by Loh in the context of MD simulations. We used classical MD simulations to study the desalination performance of nanoporous bicrystalline hBN using the open-source Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) package. The simulation system for water desalination is illustrated in Figure 1, in which nanoporous hBN was placed parallel to the x–y plane. We used a simulation box measuring 160 Å in the z-direction and periodic in the x–y directions with a cross-sectional area of \( \sim 31 \times 31 \) Å². The nanoporous hBN sheet was fixed at \( z = 0 \) Å, and rigid graphene pistons were placed at \( z = -75 \) and 18.5 Å. The feed-side region of the simulation box was filled with saline water having 22 Na⁺ ions, 22 Cl⁻ ions, and 2000 water molecules, leading to a salt concentration of 35.7 g L⁻¹, close to the value observed in seawater. The permeate (i.e., pure water) side was filled with 500 water molecules. We verified that the use of a larger number of water molecules on the permeate side did not affect our results. Indeed, the water flow rates through a nanoporous monocrystalline hBN membrane at 50 MPa feed pressure were found to be the same when 500 and 2000 water molecules were present on the permeate side, as shown in Figure S1 in Section S1 of the Supporting Information.

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![Figure 1](https://doi.org/10.1021/acs.jpcb.1c09287)
of desalination and by other researchers. The TIP4P/2005 water model was used to represent water molecules, whereas Lennard-Jones (LJ) and Coulombic interatomic potentials were used for all of the intermolecular interactions. The parameters for LJ and Coulombic interatomic potentials were taken from Konatham et al. for carbon atoms, Govind Teter and Hutter for the sodium and chloride ions. These are tabulated in Section S3. To calculate the interactions between unlike atoms in the system, geometric mean combining rules, \( \sigma_{ij} = (\sigma_i \sigma_j)^{1/2} \) and \( \epsilon_{ij} = (\epsilon_i \epsilon_j)^{1/2} \), were used, where \( \sigma \) represents the distance at which the interatomic LJ potential is zero and \( \epsilon \) represents the LJ well-depth parameter. In Section S4, we present a more detailed discussion on the choice of force fields for hBN, water molecules, and salt ions (see, e.g., refs 14 and 53).

**Partial Charge Calculations.** To calculate the partial charges, the geometry of monocrystalline and bccrystalline nanoporous hBN membranes was optimized using the Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm, leading to a maximum force of 0.0003 hartree bohr⁻¹ on the atoms. The DFT calculations were performed using the cp2k package and the Perdew–Burke–Ernzerhof (PBE) exchange–correlation functional with double-\( \zeta \) (short-range) valence basis sets for the B and N atoms. The nuclei and core electrons were modeled using the Goedecker–Teter–Hutter pseudopotentials. Subsequently, partial charges on B and N atoms were calculated using the density-derived atomic point (DDAP) charge algorithm developed by Blöchl. After calculating the partial charges, the electrostatic potential plots in Figures S5 and S6 were prepared by calculating the electrostatic interaction between a unit test charge and the nanoporous hBN membrane (see Figure S3a in Section S5) using the group/group command in LAMMPS. The same group/group command was also used to plot the contours of the interfacial interactions between a single, tangential water molecule and the nanoporous hBN membrane, as shown in Figures 12 and 13. The simulation setup used to calculate these interactions is shown in Figure S3b in Section S5.

**RESULTS AND DISCUSSION**

**GB Misorientation Angles and Nanopore Shapes in hBN.** In this work, we modeled water and ion permeation through four different hBN membranes: (i–iii) bccrystalline nanoporous hBN with symmetric tilt GBs having misorientation angles (\( \theta \)) of (i) 13.2°, (ii) 21.8°, and (iii) 32.2° and (iv) monocrystalline nanoporous hBN (i.e., without any GB), as shown in Figure 2. We considered the monocrystalline hBN membrane to compare our findings with previously reported results and to quantify the effect of GBs on the desalination performance of nanoporous hBN. The nomenclature of the GB structures considered and details regarding their repeat length are described in Section S6. The bccrystalline hBN configurations were created using the sewing method, which generates pairs of pentagon–heptagon (5/7) dislocations at the junctions of the two misoriented crystals of hBN, as shown in Figure 2. Similar types of GB structures in hBN and graphene have been seen experimentally and predicted theoretically in various studies. We chose these three misorientation angles because they cover varying linear dislocation densities (i.e., the number of (5/7) dislocation pairs on the GB per unit length) from low to high (\( \sim 0.91, 1.5, \) and 2.24 nm⁻¹).

Nanopores were considered at the GB because it is more likely for extended defects, such as nanopores, to form there. We considered roughly triangular nanopores with nitrogen-terminated edges because triangular, boron-deficient defects are more likely to form in hBN, as seen experimentally and predicted theoretically by previous studies. For nanoporous monocrystalline hBN, we considered a nanopore formed by removing 10 B atoms and 6 N atoms from the hBN lattice, leading to a total of 16 removed atoms (Figure 2a,b).
Indeed, in previous work, Govind Rajan et al.\textsuperscript{72} cataloged the most-probable nanopore shapes in hBN using kinetic Monte Carlo simulations, DFT calculations, and graph theory and predicted triangular shapes of nanotubes with nitrogen atoms at their edges to be the most prevalent in hBN. Further, Kozawa et al.\textsuperscript{73} predicted that triangular shapes of nanopores are the most kinetically favorable defects in hBN when a perfect square number of atoms (16 here) was removed. The choice of considering a triangular nanopore in hBN is also substantiated by the experimental observation of triangular vacancy defects in hBN.\textsuperscript{74,75} The triangular nanopore formed by removing 25 atoms (the next perfect square after 16) was not considered because of the tradeoff between the increased water flux and reduced ion rejection. Indeed, while the water flux can be improved by considering a larger nanopore, the ion rejection ability of the membrane will severely deteriorate in such a scenario. Thus, to investigate the overall efficiency of a nanoporous membrane for desalination purposes, a tradeoff between water flux and ions rejection is very crucial. For the 13.2°-misoriented bicrystalline hBN, equal numbers of B and N atoms as in the monocrystalline case (10 and 6, respectively) were removed to form the nanopore (Figure 2c,d); yet, the area of the nanopore was slightly larger (27.6 versus 26.4 Å²) due to the presence of the GB. The calculation of the nanopore area is explained in Section S7.

Note that our estimate of 26.4 Å² for the area of the nanopore in monocrystalline hBN formed by removing 10 B and 6 N atoms from the hBN lattice was similar to the estimate of 29.1 Å² obtained by Davoy et al.\textsuperscript{77} For the 21.8°-misoriented bicrystalline hBN, nine B atoms and five N atoms were removed to form a roughly triangular nanopore (Figure 2e,f); the resulting nanopore area was the smallest at 23.6 Å². Finally, for the 32.2°-misoriented bicrystalline hBN, 10 B atoms and 5 N atoms were removed to form a roughly triangular nanopore (Figure 2g,h), leading to an intermediate nanopore area of 25.8 Å². It was evident that the presence of a GB affects the nanopore area and shape. Later in the article, we also discuss the water desalination performance of these nanopores after normalization by the nanopore area. In all of the considered cases, the nanopore concentration (i.e., pore density) in the hBN layer was ~0.09–0.10 nm⁻² (see the caption of Figure 2). This is a large value considering that almost 10⁷ nanopores would be present in 1 m² area of the membrane. Nevertheless, our estimates of the per-pore permeance/permselectivity could simply be multiplied by the actual pore density to obtain the membrane permeance/permselectivity for membranes with a lower number of pores per unit area.\textsuperscript{76} In Table 1, we list the areas of the nanopores considered, their equivalent circular diameters, and their aspect ratios, as quantified by the ratio of the minimum to maximum Feret diameter of the nanopore (see Section S7 for more details). The Feret diameter, also known sometimes as the caliper diameter, is the distance between the jaws of a caliper used to measure the size of an object. Note that the aspect ratio, as defined above, lies between 0.0 and 1.0. The limiting value of 1.0 corresponds to a circle and that of 0.0 to a line segment; the aspect ratio of an equilateral triangle, equaling the ratio of its height to its side length, is \( \sqrt{3}/2 = 0.87 \). Thus, the lower the aspect ratio of a nanopore is, the more elongated it is. From Table 1, we can see that the extent of elongation of the considered nanopores is in the following order: monocrystalline hBN < 13.2°-misoriented hBN < 21.8°-misoriented hBN < 32.2°-misoriented hBN.

### Partial Charge Calculations and Validation of the Resulting Electrostatic Potential with DFT

As discussed above, hBN membranes used for water desalination have intentionally induced geometrical defects such as nanopores and inadvertently induced geometrical defects such as GBs. These geometric defects in hBN alter the partial charges on B and N atoms, ultimately affecting the electrostatic interactions between water and hBN. To quantify this effect, we calculated the partial charges on B and N atoms in the hBN membranes considered here using the DFT-based DDAP charge algorithm (see Partial Charge Calculations in the Methods section for more details). Specifically, partial charges were calculated using nine different sets of DDAP parameters, as described in Section S8. Here, we focus on results obtained using the default DDAP parameters and the “best” DDAP parameters (see below). The contours plots of the partial charges calculated using the default and best DDAP parameters are indicated in Figures 3a–d and 4a–d, respectively, for the four cases (i)–(iv) discussed above. It can be inferred from Figures 3b–d and 4b–d that in bicrystalline hBN membranes, B atoms adopt negative charges and N atoms adopt positive charges when DDAP parameters are altered from their default values to their best values (see Section S8 for the parameter values). In contrast, no such sign reversal in the partial charges of B and N atoms takes place in a monocrystalline membrane when using the best DDAP parameters, as seen by comparing Figures 3a and 4a. This sign reversal, found essential to reproduce the DFT-predicted electric potential, as discussed below, could be caused by a polarizing electric field at the GB parallel to the hBN surface and perpendicular to the GB and should be probed more deeply in the future.

To validate the DFT-predicted partial charges, we also calculated the electrostatic potential generated by the total DFT charge density (electrons and ions) in the hBN membrane. This was achieved by writing a cube file using the V_HARTREE_CUBE section in cp2k. The electrostatic potential values at points directly above the center of the nanopore were plotted against the perpendicular distance from the surface of the hBN sheet for both monocrystalline and bicrystalline configurations, as shown in Figure 5. To obtain the potential created by the partial charges on B and N atoms, a unit test charge was placed at the center of the nanopore of the hBN membrane, as depicted in Section S5. This unit test charge was moved in the direction perpendicular to the hBN surface, and the electrostatic interactions between the hBN layer and the test charge were obtained using single-point calculations in the LAMMPS package.\textsuperscript{41} The resulting electrostatic potential was compared with the DFT potential, as shown in Figure 5. It can be inferred from Figure 5a–d that the electrostatic potentials calculated using the partial charges with default DDAP parameters do not agree with the DFT potential. In contrast, the electrostatic potentials calculated using the partial charges with the “best” DDAP parameters for

### Table 1. Geometrical Properties of the Four Nanopores Considered in This Work

| configuration | area (Å²) | equivalent circular diameter (Å) | aspect ratio |
|---------------|-----------|---------------------------------|--------------|
| monocrystalline | 26.4 | 5.80 | 0.91 |
| 13.2° | 27.6 | 5.93 | 0.84 |
| 21.8° | 23.6 | 5.49 | 0.78 |
| 32.2° | 25.9 | 5.74 | 0.62 |
nanoporous monocrystalline and bicrystalline (21.8°- and 32.2°-misoriented) hBN (see Figure 5a,c,d) were in excellent agreement with the DFT potential. In the case of the 13.2°-misoriented bicrystalline hBN membrane, there was a minor deviation between the DFT potential curve and the electrostatic potential curve calculated using the partial charges with the best DDAP parameters. We show in Section S8 that it is not possible to eliminate these differences by tuning the partial charges. Nevertheless, later in the article, we show that this minor deviation between the DFT and partial-charge-based potentials does not affect the main conclusion of our work. It is also seen in Figure 5 that the electrostatic potential is the highest at the center of the pore (the hBN layer is placed at z = 0 Å), with a symmetric decrease in potential, on either side, as one moves away from the hBN layer.

**Water Flow Rate through Nanoporous Monocrystalline and Bicrystalline hBN.** After calculating and validating the partial charges, MD simulations were performed to investigate the desalination performance of nanoporous monocrystalline and bicrystalline hBN membranes. The simulation system for water desalination is illustrated in Figure 1 and consists of a nanoporous hBN layer, two rigid graphene pistons, water molecules, and sodium (Na\(^+\)) and chloride (Cl\(^-\)) ions. To analyze the desalination performance of these membrane configurations, the number of water molecules that permeated through the membrane \((N_w)\) was counted and plotted as a function of time at different feed pressures ranging from 50 to 200 MPa, as shown in Figure 6. The permeate pressure was maintained at 0.1013 MPa (i.e., 1 atm) in all cases. All simulations for water permeation were run until 200 water molecules (10% of the total water molecules on the feed side) permeated through the membrane. This was done so that the salinity of the water in the feed side was not significantly affected, thereby preventing large variations in chemical potential gradients during the water and ion permeation process. Therefore, the simulation times varied as a function of the applied pressure (as shown in Figure 6) and increased from ~2 to ~9 ns as the applied pressure decreased from 200 to 50 MPa. Note that, in some of the previously published studies, simulations were performed for a longer time (~30 ns), thereby significantly affecting the salinity of water on the feed side. One can observe from the plotted trend in Figure 6 that in all of the membrane configurations, the number of permeating water molecules followed a linear trend with simulation time, which is a signature of constant pressure and chemical potential driving force. Moreover, the number of permeating water molecules significantly depended on the imposed pressure. As the imposed pressure increased, the value of \(N_w\) at a fixed time also increased for all of the hBN configurations.

After plotting \(N_w\) versus time, we calculated the water flow rate in each case to quantify the desalination performance. The water flow rate is defined as the number of permeated water molecules divided by the time taken for permeation. In this work, the water flow rate was calculated using two methods that are described in Section S9, namely, (a) using the slope of a linear fit of the \(N_w\) versus time plot and (b) using the total number of permeated water molecules divided by the total time taken for their permeation. After comparison of calculated water flow rates obtained using the two methods in Section S9,
Figure 4. Partial charge distribution (in elementary charge units (e)) calculated using the “best” DDAP parameters for various configurations: (a) monocrystalline, (b) 13.2°-misoriented bicrystalline, (c) 21.8°-misoriented bicrystalline, and (d) 32.2°-misoriented bicrystalline nanoporous hBN. Five-membered rings are colored in magenta, and seven-membered rings are colored in green.

Figure 5. Electrostatic potential as a function of perpendicular distance from the surface of the membrane for various configurations: (a) monocrystalline, (b) 13.2°-misoriented bicrystalline, (c) 21.8°-misoriented bicrystalline, and (d) 32.2°-misoriented bicrystalline nanoporous hBN. Values calculated using DFT (purple), partial charges based on the default DDAP parameters (gray), and partial charges based on the best DDAP parameters (orange) are shown. The hBN membrane is placed at \( z = 0 \) Å in each case.
we adopted method (a) to calculate the water flow rates in the rest of the article because it better accounts for temporal fluctuations in the water flow rate. All of the water flow rates and ion selectivities reported in this article were obtained as the average value from five independent simulation runs using different initial aqueous configurations and velocity distributions. The error bars indicated in each case represent the standard deviations from such collections of five runs.

To compare the calculated water flow rates with previously reported results, we plotted the obtained water flow rates as a function of the effective pressure drop and superimposed previously published results on the same plot, as illustrated in Figure 7. The effective pressure drop is given as $P_{\text{eff}} = \Delta P - \Delta \Pi$, where $\Delta P$ and $\Delta \Pi$ represent, respectively, the difference in the applied pressures and the difference in the osmotic pressures between the feed and permeate sides. Note that the $\Delta \Pi$ term has been neglected in previous simulation work on coupled water and ion transport through nanoporous hBN. This term is calculated using the van’t Hoff equation, $\Delta \Pi = iRT\Delta c$, where $i$ is the van’t Hoff factor (2 due to complete dissociation of NaCl), $\Delta c$ is the difference in the molar concentrations of the solute on the feed and permeate sides ($610.863 \text{ mol m}^{-3}$ or $35.7 \text{ g L}^{-1}$), $R$ is the universal gas constant (8.314 Pa m$^3$ mol$^{-1}$ K$^{-1}$), and $T$ is the temperature of the system (298.15 K), whence the calculated value of the osmotic pressure difference is 3.03 MPa. The three feed-side pressures, i.e., 50, 100, and 200 MPa, lead to effective pressure values of 46.87, 96.87, and 196.87 MPa, respectively. Similar values of pressure drop have been considered in several theoretical studies.$^{17,18}$ Moreover, such high feed pressures (closer to 50 MPa) are currently being explored experimentally.$^{17}$ Nevertheless, later in the article, we also report water flow rates versus effective pressure plots for nanoporous monocrystalline hBN membranes. The calculations in this work were carried out using two different interatomic potentials to model hBN flexibility—the Tersoff force field proposed by Albe et al.,$^{45}$ with the results in purple, and the valence force field proposed by Govind Rajan et al.$^{51}$ with the results in yellow. Results from Garnier et al.$^{17}$ and Gao et al.$^{18}$ are shown in green and gray, respectively. Lines are only visual guides and do not indicate any fit.
permeabilities, which are normalized by the pressure decrease, such that our results are independent of the applied pressure.

It can be inferred from Figure 7 that the water flow rates predicted in this work for nanoporous monocrystalline hBN are comparable with previously published work. Note that no previous calculations are available for water and ion permeation through nanoporous bccrystalline hBN. Nevertheless, variations were observed from previously predicted water flow rates of nanoporous monocrystalline hBN due to different force-field parameters employed and the shape and size of the nanopores considered in the previous work. For example, Gao et al. 18 considered the same nanopore as that used in this work but used different models/parameters, including for water (TIP3P), hBN−water Lennard-Jones (LJ) interactions, partial charges on B and N atoms, and the flexibility of hBN (universal force field). In contrast, Garnier et al. 17 used the TIP4P/2005 water model with the same LJ parameters as employed by Gao et al. 18 but considered an elongated nanopore. Since not only the size of the nanopore but also its shape affects the permeation of water, 15 it is reasonable that the water flow rate predicted by Garnier et al. 17 is much higher than that predicted by Gao et al. 18 It can also be seen in Figure 7 that the force field used to model the flexibility of nanoporous monocrystalline hBN does not affect water permeation significantly, as seen from our results shown in purple (using the Tersoff force field proposed by Albe et al. 55) and yellow (using the valence force field proposed by Govind Rajan et al. 51). After comparison of the water flow rates of nanoporous monocrystalline hBN membranes predicted by different force fields, the Tersoff force field was used to model the flexibility of nanoporous monocrystalline and bicrystalline hBN membranes in the rest of this work because the force field by Govind Rajan et al. 51 cannot be used to model B–B and N–N bonds that are seen at GBs.

Effect of GBs on the Water Flow Rate, Water Flux, and Water Permeability through Nanoporous hBN. We next analyzed the effect of GBs on the desalination performance of nanoporous bccrystalline hBN membranes. As seen before, in Figure 6, the number of water molecules passing through nanoporous monocrystalline and bicrystalline hBN membranes was plotted against the simulation time at different feed pressures. Subsequently, we calculated the water flow rate for various bccrystalline hBN membrane configurations and plotted the values against the effective pressure, as shown in Figure 8a. One can infer from Figure 8a that the water flow rate follows an almost linear trend with the effective pressure; as the effective pressure increases, the water flow rate also increases for all of the hBN membrane configurations. It is evident from Figure 8a that the lower-angle misoriented bicrystalline hBN membrane (with 13.2° misorientation angle) shows an improved water flow rate as compared to the monocrystalline hBN configuration, by ∼30% at 46.87 MPa effective pressure. This finding can be attributed to the higher equivalent circular diameter (5.93 Å) and lower aspect ratio (0.84) of the nanopore in 13.2°-misoriented bicrystalline hBN, as compared to the nanopore of 5.80 Å diameter and 0.91 aspect ratio in monocrystalline hBN (see Table 1). On the other hand, the water flow rate of the higher-angle misoriented bicrystalline hBN membranes is comparable with that for the monocrystalline configuration. This observation is despite the fact that the nanopores in the higher-angle misoriented bicrystalline hBN membranes had a lower area (equivalent circular diameter) than the nanopore considered in monocrystalline hBN, thus indicating that GBs intrinsically enhance water permeation through nanoporous hBN. The underlying reason could be attributed to the lower aspect ratio of the nanopores in 21.8°- and 32.2°-misoriented bicrystalline hBN, as compared to the nanopore in monocrystalline hBN, as seen in Table 1.

As mentioned above, the nanopore shape significantly affects water and ion permeation through nanoporous hBN. Thus, we maintained an approximately triangular shape of the nanopore in all of the bicrystalline configurations, as in the monocrystalline configuration. Nevertheless, due to this constraint, the sizes of the nanopores slightly varied in the bicrystalline configurations as compared to those in the monocrystalline configuration. To analyze the intrinsic effect of GB configurations on the desalination performance of nanoporous bicrystalline hBN, the water flux (i.e., the water flow rate normalized by the nanopore area) was calculated and plotted

Figure 8. (a) Water flow rate and (b) water flux versus effective pressure for nanoporous monocrystalline and bicrystalline hBN membranes. Lines are only visual guides and do not indicate any fit.
as a function of the effective pressure, as shown in Figure 8b. It can be deduced from Figure 8b that the water flux follows a similar trend to that followed by the water flow rate. Nevertheless, the improvement in the water flux was slightly smaller (≈24%) at 46.87 MPa effective pressure, as compared to the improvement in the water flow rate, in the case of the 13.2°-misoriented bicrystalline hBN membrane. On the other hand, the water fluxes through the 21.8°- and 32.2°-misoriented bicrystalline hBN membranes were closer to the monocrystalline hBN case.

The water permeability in L cm⁻² day⁻¹ MPa⁻¹, defined as the volume of water permeated per unit time, membrane area, and pressure, was also calculated at 46.87 MPa effective pressure and is plotted in Figure 9. It can be seen from Figure 9 that the improvement in the water permeability was more remarkable (≈47%) at 46.87 MPa effective pressure, as compared to the improvement in the water flow rate, in the case of the 13.2°-misoriented bicrystalline hBN membrane. This extra improvement in the permeability of the 13.2°-misoriented bicrystalline hBN membrane is attributed to its lower surface area (1000 Å²), as compared to the higher surface area of the monocrystalline hBN membrane (1136 Å²). On the other hand, the water permeabilities through the 21.8°- and 32.2°-misoriented bicrystalline hBN membranes are almost identical to that of the monocrystalline hBN membrane.

Nevertheless, the water permeability estimate of ∼12–18 L cm⁻² day⁻¹ MPa⁻¹ for nanoporous hBN is comparable in order of magnitude to estimates obtained for graphene, MoS₂, and MOF membranes considering pore areas similar to those in our study (25–30 Å², see Table 1).

Comparison of Our Results with Experimental Data and Avenues for Future Work. The calculated values of water permeability for monocrystalline and bicrystalline hBN membranes are in the range of 12.0–17.9 L cm⁻² day⁻¹ MPa⁻¹, which are several times higher than those of current commercial RO membranes (∼0.1 L cm⁻² day⁻¹ MPa⁻¹, see ref 6) and better than that of a graphene filter (∼5.9 L cm⁻² day⁻¹ MPa⁻¹ measured in an experimental study). However, as mentioned before, the pore density considered in our work is ∼10¹⁷ nm⁻². This value, although comparable to what is considered in other simulation studies, is about an order of magnitude higher than the value of 10⁶ nm⁻² achieved experimentally in graphene. This observation indicates that one may reasonably achieve anywhere between 1.2 and 1.8 L cm⁻² day⁻¹ MPa⁻¹ of performance using an hBN membrane. (A better performance would require the generation of more pores per unit area in hBN.) In contrast, the experimentally measured values of water permeance for amino-functionalized nanoporous hBN are in the range of 14.9 to ∼48 L cm⁻² day⁻¹ MPa⁻¹ for membranes of thickness 2000 and 400 nm, respectively. The variation in the water permeability by a factor of 2–3 between the simulated and experimental results can be attributed to the larger sizes of the nanopores in the experimental samples. Indeed, the sizes of the nanopores in the experimentally synthesized hBN used by Chen et al. are in the range of 8.0–18.3 Å, which are larger than the sizes of the nanopores considered in our work (5–6 Å). Note that the study of Chen et al. considered lamellar hBN membranes, i.e., membranes synthesized using exfoliated hBN flakes. In addition, work is needed to understand how edge functionalization affects the sizes of nanopores in hBN and, consequently, water and ion transport through nanopores in the material. The investigation of edge functional groups would also require the development of force-field parameters to describe functionalized hBN edges.

Quantifying the Free Energy Barriers for Water Permeation. When water molecules pass through a nanopore in the hBN membrane, they have to surmount a free energy barrier. To further understand the water permeation mechanism through nanopores, we calculated the free energy profile or potential of mean force (PMF) of water molecules using the Boltzmann sampling method. According to the Boltzmann sampling method, the free energy or PMF is given as $F(z) = -RT \ln \rho(z)$, where $R$ represents the universal gas constant, $T$ represents the temperature, and $\rho(z)$ represents the density at position $z$ in the system. After obtaining the water density profiles from an equilibrium simulation with equal feed and permeate pressures of 1 bar, the free energy profiles were plotted for nanoporous monocrystalline and bicrystalline hBN membranes, as shown in Figure 10.

It can be inferred from Figure 10 that the free energy profile of the water molecules is approximately constant far away from the membrane, which is placed at $z = 0$, in all cases. At the position of membrane ($z = 0$), a large increase in the free energy is observed. This free energy enhancement at the nanopore represents the energy barrier for water permeation from the feed side to the permeate side. It can be observed from Figure 10 that the lower-angle misoriented bicrystalline hBN membrane shows a lower energy barrier, which causes higher water flux, as compared to the higher-angle misoriented bicrystalline configuration. In contrast, the 21.8°-misoriented bicrystalline hBN membrane shows a higher energy barrier, such that the water flux is lower. Overall, the trends presented by the free energy barriers ($21.8° > 0° > 32.2° > 13.2°$) in Figure 10 match the trends presented by the water fluxes ($21.8° < 0° < 32.2° < 13.2°$), where a misorientation of 0° indicates nanoporous monocrystalline hBN. Moreover, these results support the observation that, even after accounting for differences in nanopore areas, the 13.2°-misoriented bicrystalline hBN allows increased water flux through the hBN membrane. In this regard, future work could investigate the coupled role of temperature and grain boundaries in modulating water and ion transport through 2D nanopores.
by simulating the desalination process at various system temperatures. Such an approach would enable the estimation of activation barriers for water permeation using an alternative method, and the ensuing results could be compared with the PMF-based approach presented here.

**Effect of GBs on Ion Rejection by Nanoporous hBN.**

Apart from the water flux, the extent of rejection of Na\(^+\) and Cl\(^-\) ions from water is a crucial criterion for any desalination membrane. We counted the percentage of Na\(^+\) and Cl\(^-\) ions that were rejected in each simulation run for various membrane configurations at different effective pressure values, as summarized in Tables 2 and 3, respectively. It can be deduced from Table 2 that, in only the monocrystalline membrane configuration, sodium rejection is greater than 99% (corresponding to a maximum of a single Na\(^+\) ion permeating in one out of five independent simulation runs). For the bicrystalline membranes, Na\(^+\) rejection follows the order 32.2° > 21.8° > 13.2°, with the maximum possible rejection being 97.3%. The 13.2°-misoriented bicrystalline membrane shows the least Na\(^+\) rejection as compared to monocrystalline hBN configuration, which is only 92.7% at 46.87 MPa effective pressure. Nevertheless, we observe from Table 3 that as such no Cl\(^-\) ions (with an ionic radius of 1.81 Å\(^{-}\)) pass through the membrane (except in very few runs) due to their larger size (note that the ionic radius of Na\(^+\) is 0.99 Å\(^{-}\)). Since a high ion rejection (>99%) is an important requirement and is considered even more significant than high water permeability for commercial RO membranes,\(^{80}\) our findings indicate that the presence of GBs in nanoporous hBN can compromise their water desalination performance through a decrease in ion rejection.

**Effect of Interfacial Electrostatic Interactions on Water Desalination Performance.** Although, intuitively, interfacial electrostatics should play an important role in modulating water and ion permeation, no previous study has investigated the effect of these electrostatic interactions on the desalination performance of nanoporous hBN. In this regard, the method used to assign partial charges to the membrane atoms, based on DFT calculations, is crucial. In previous work, authors have either used Mulliken population analysis\(^1\) (e.g., Davoy et al.\(^{15}\) and Garnier et al.\(^{17}\)) or the Hirshfeld charge scheme\(^2\) (e.g., Gao et al.\(^{19}\)) to obtain the charges on B and N atoms. Yet others have used the density-derived electrostatic and chemical (DDEC) method\(^{20}\) and electrostatic potential fitting (ESP) method (e.g., Jafarzadeh et al.\(^{10}\)) to calculate partial charges. In previous work, we showed that ESP-based charges are not able to predict correctly the electrostatic potential above defects in hBN.\(^{84}\) In Section S10, we show that DDAP (using default parameters), Hirshfeld, Mulliken, and DDEC partial charges are also not suitable for predicting the electrostatic potential above nanopores in hBN. Instead, only the DDAP charges with customized parameters are found to be accurate for this purpose. Finally, Loh\(^4\) investigated the desalination performance of nanoporous hBN membrane using the partial charges on B and N atoms from periodic BN nanotubes, which, as we show below, may underpredict the water permeation rate through nanoporous hBN. To this end, here, we analyzed the effect of electrostatic interactions on the desalination performance of monocrystalline and bicrystalline nanoporous hBN. To evaluate the effect of interfacial electrostatic interactions, we calculated the water flow rate with three different sets of partial charges on the B and N atoms in the hBN membrane: (i) partial charges calculated using DFT and the DDAP method, (ii) bulk partial charges on each B (q = +0.907 e) and N atom (q = −0.907 e) (these charges were calculated by Govind Rajan et al.\(^{51}\) for monocrystalline hBN nanosheets) and (iii) by taking zero charges on each B and N atom, i.e., when the interfacial electrostatic interactions are zero. After calculating the water flow rate for different sets of partial charges, we plotted these results against the effective pressure for various nanoporous monocrystalline and bicrystalline hBN membranes, as shown in Figure 11. The results for the water flow rate are also tabulated in Table 4 for the different sets of partial charges considered at 196.87 MPa effective pressure. It can be inferred from Figure 11 and Table 4 that in all of the nanoporous hBN membranes, the water flow rate is significantly affected by the interfacial electrostatic interactions. The values of water flow rate were the highest when the altered partial charges on B and N atoms were calculated using DFT-based simulations and the DDAP method, whereas the values of water flow rate were the lowest when bulk charges (charges in monocrystalline hBN

![Figure 10. Free energy profile, i.e., the PMF, along the flow direction (z-direction) for nanoporous monocrystalline and bicrystalline hBN membranes of varying misorientation angles.](https://doi.org/10.1021/acs.jpcb.1c09287)
nanosheets) on B and N atoms were used. (Note that, in the latter case, the hBN membrane is charged, due to the presence of an unequal number of B and N atoms in it. Accordingly, MD simulation packages add a uniform background charge to the system such that the net charge on the simulation box is zero.) The water flow rates calculated without considering electrostatic interactions (i.e., considering zero partial charges on B and N atoms) were found to lie in between cases (i) and (ii). We also see in Table 4 that a maximum of 69.1% improvement in the water flow rate was observed when compared with the flow rate predicted using zero partial charges and 297.4% improvement was observed when compared with the flow rate predicted using bulk charges. Overall, we conclude that the calculated partial charges must be accurate enough, as the water flow rate is significantly affected by the interfacial electrostatic interactions. Moreover, the water flow rate reduces significantly if the hBN sheet is charged. Note that, in our simulations, the monocrystalline, 13°-misoriented bicrystalline and 21.8°-misoriented bicrystalline hBN configurations have four fewer B atoms than N atoms, leading to a surface charge density of \(-0.051\) to \(-0.059\) C m\(^{-2}\). On the other hand, the 32.2°-misoriented hBN membrane has five fewer B atoms than N atoms, resulting in \(-0.066\) C m\(^{-2}\) of surface charge. It can also be seen from Table 4 that the water flow rate is maximum in the 13.2°-misoriented bicrystalline membrane as compared to other membrane configurations even when we are considering zero or bulk charges. Therefore, the water flow rate is always maximum in

| pressure (MPa) | monocrystalline nanoporous hBN | bicrystalline nanoporous hBN |
|---------------|--------------------------------|----------------------------|
| 46.87         | 100 ± 0.00                     | 99.09 ± 2.03                |
| 96.87         | 100 ± 0.00                     | 100 ± 0.00                  |
| 196.87        | 99.09 ± 2.03                   | 100 ± 0.00                  |

**Table 4. Water Flow Rate through Monocrystalline and Bicrystalline hBN Membranes for Different Partial Charges at 196.87 MPa Effective Pressure**

| configuration | water flow rate (molecule ns\(^{-1}\)) | % improvement in water flow rate using DDAP charges |
|---------------|----------------------------------------|---------------------------------------------------|
|               | DFT charges                            | zero charges                                      | bulk charges                                      | compared with zero charges | compared with bulk charges |
| monocrystalline | 102.8                                 | 67.4                                              | 35.7                                              | 52.6                          | 188.3                        |
| 13.2°          | 131.8                                 | 89.6                                              | 36.9                                              | 47.2                          | 257.4                        |
| 21.8°          | 86.7                                  | 51.7                                              | 24.6                                              | 67.9                          | 253.3                        |
| 32.2°          | 106.2                                 | 62.8                                              | 26.7                                              | 69.1                          | 297.4                        |

Figure 11. Water flow rate versus effective pressure plots for various configurations: (a) monocrystalline, (b) 13.2°-misoriented bicrystalline, (c) 21.8°-misoriented bicrystalline, and (d) 32.2°-misoriented bicrystalline nanoporous hBN membranes.
the 13.2°-misoriented bicrystalline membrane, irrespective of whether we consider DFT, bulk, or zero charges for the B and N atoms. This finding indicates that our conclusion regarding the water permeability being the highest through the 13.2°-misoriented bicrystalline hBN membrane is not affected by the minor difference between the DFT and partial-charge-based potential, as seen in Figure 5b.

To further investigate the physics behind the effect of interfacial electrostatic interactions, we plotted the contours of interfacial interactions for nanoporous monocrystalline and 32.2°-misoriented bicrystalline hBN membranes using different sets of partial charges, as shown in Figures 12 and 13. To plot the contours of interfacial interactions between the nanoporous hBN membrane and water molecule, initially, a water molecule was placed at the corner of the nanoporous hBN membrane at a distance of 3 Å above the surface, as depicted in Section S5. Subsequently, the water molecule was moved in the lateral direction and the interaction energy was calculated in a grid above the hBN surface. The interfacial interaction contours for 13.2°- and 21.8°-misoriented bicrystalline membranes are not depicted, as they show similar trends, as observed for the 32.2°-misoriented bicrystalline membrane. It can be seen from Figures 12 and 13 that the partial charges cause positive and negative patches of electrostatic potential in the vicinity of the nanopore. Depending on the magnitude of these patches, water permeation is enhanced (using DDAP-based DFT partial charges) or impeded (using bulk partial charges). Comparing panels b and c in Figure 12 with panels d and e in the same figure, we see that the water–nanoporous monocrystalline interaction energy is lower while using DDAP-based DFT partial charges (Figure 12b,c), as compared to while using bulk partial charges (Figure 12d,e). A similar conclusion is reached for the case of 32.2°-misoriented bicrystalline nanoporous hBN, by examining panels b and c in Figure 13 and comparing them with panels d and e in the same figure. Thus, the presence of an optimal level of interfacial Coulombic interactions enhances water transport to the surface, and through to the other side of the nanopore, as in the case with DDAP-based partial charges. However, when the interfacial Coulombic interactions are too high, as in the case with bulk partial charges, the water molecules get trapped at the nanopore mouth, leading to a reduced water permeation rate.

Figure 12. Interfacial interaction energy contours (in kcal mol⁻¹) for a tangential water molecule at 3 Å from the membrane, using different sets of partial charges for a nanoporous monocrystalline hBN membrane: (a) LJ interaction energy, (b) electrostatic potential energy calculated using DDAP-based DFT charges, (c) total potential energy calculated using DDAP-based DFT charges, (d) electrostatic potential energy calculated using bulk charges, and (e) total potential energy calculated using bulk charges.
CONCLUSIONS

For water desalination membranes, large-area 2D materials are required, which inevitably will contain grain boundaries (GBs) as geometrical defects. In this work, we investigated the role of GBs and interfacial electrostatic interactions in modulating the desalination performance of bicrystalline hBN membranes using classical MD simulations supported by quantum-mechanical DFT calculations. Before investigating the desalination performance, we calculated the partial charges on each B and N atom in hBN using DFT and validated these partial charges with the help of electrostatic potential plots. The electrostatic potential calculated using DFT and that using partial charges are in good agreement for monocrystalline and bicrystalline configurations. By investigating water and ion permeation using MD simulations, we concluded that, although the lower-angle (13.2°) misoriented bicrystalline hBN membrane showed improved water flow rate by ~30%, Na\(^+\) rejection was reduced by ~6% as compared to monocrystalline hBN. The finding regarding increased water flow persisted even after correcting the water flow rates for the nanopore area, i.e., considering the water flux through the investigated nanopores. In fact, the water flow rate and flux through higher-angle (21.8 and 32.2°) misoriented bicrystalline hBN was found comparable to that through nanoporous monocrystalline hBN, despite them having smaller nanopore areas. We showed that these nanopores have a lower aspect ratio, thus pointing to the role of the nanopore shape in modulating water flux, as well as ion rejection. Indeed, the increased water flow rate was accompanied by a significant decrease in Na\(^+\) rejection by the membrane. We also deduced that the values of the water flow rate were the highest when altered partial charges on B and N atoms were calculated using DDAP-based DFT calculations, whereas the values of the water flow rate were the lowest when bulk partial charges (i.e., the charges in a monocrystalline hBN nanosheet) on B and N atoms were used. This implies that surface charge on the membrane reduces the rate of water permeation. Additionally, the water flow rates calculated without considering interfacial electrostatic interactions, i.e., by taking zero partial charges on B and N atoms, were in between the two cases discussed above. Overall, our investigation of the role of GBs and interfacial electrostatic interactions in modulating the desalination performance of nanoporous bicrystalline hBN informs the use of a large-area hBN membrane in seawater desalination applications. Specifically, we find that the presence of GBs and surface charge may be deleterious for, respectively, ion

![Figure 13](https://doi.org/10.1021/acs.jpcb.1c09287)
rejection and water permeation through nanoporous hBN membranes. Thus, monocrystalline nanoporous hBN should be preferred for synthesizing water desalination membranes. To conclude, we hope that future studies consider the effect of GBs, which are prevalent in large-area membranes, on the desalination performance of other nanoporous 2D materials as well, while realistically modeling interfacial electrostatic interactions.

## ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcb.1c09287.

Water flow rate for nanoporous monocrystalline hBN membrane at 50 MPa feed pressure when the permeate side has 500 and 2000 water molecules; convergence of energy and temperature during equilibration; parameters for the LJ and Coulombic interatomic potentials; choice of the force fields for hBN, water molecules, salt ions, and interfacial interactions between hBN and water; model used to calculate the interfacial interactions between a nanoporous hBN membrane and a unit test charge/tangential water molecule; nomenclature and repeat length of the grain boundaries; calculation of the areas, equivalent circular diameters, and aspect ratios of the various nanopores considered; tuning of partial charges and validation of the resultant electrostatic potential for 13.2°-misoriented bicrystalline nanoporous hBN; comparing two different methods for water flow rate calculation; and comparison of the classical electrostatic potentials calculated using DDAP, Hirshfeld, Mulliken, and density-derived electrostatic and chemical (DDEC) partial charges with the DFT-derived potential (PDF).

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**Notes**

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