RaD-VIO: Rangefinder-aided Downward Visual-Inertial Odometry

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Abstract—State-of-the-art forward facing monocular visual-inertial odometry algorithms are often brittle in practice, especially whilst dealing with initialisation and motion in directions that render the state unobservable. In such cases having a reliable complementary odometry algorithm enables robust and resilient flight. Using the common local planarity assumption, we present a fast, dense, and direct frame-to-frame visual-inertial odometry algorithm for downward facing cameras that minimises a joint cost function involving a homography based photometric cost and an IMU regularisation term. Via extensive evaluation in a variety of scenarios we demonstrate superior performance than existing state-of-the-art downward facing odometry algorithms for Micro Aerial Vehicles (MAVs).

I. SUPPLEMENTARY MATERIAL

Representative video: https://youtu.be/gmFKWQCd1us

II. INTRODUCTION AND RELATED WORK

Recent advances in optimisation based monocular visual-inertial SLAM algorithms for MAVs have made great strides in being accurate and efficient [1]. However, in practice, these algorithms suffer from three main failure modalities—sensitivity to initialisation, undergoing motion that renders the state unobservable, and, to a lesser extent, inability to handle outliers within the optimisation. The first arises from the need for translation to accurately triangulate feature landmarks and being able to excite all axes of the accelerometer to determine scale. The second is a fundamental limit of the sensor characteristics, robot motion, and the environment, most often caused by motion in the camera direction and an absence of texture information. The third is often an artifact of sliding windows necessitated by the constraints imposed by limited compute on aerial platforms.

We believe that in order to have robust and resilient closed loop flight it is imperative to have complementary sources of odometry. Towards this, we present an algorithm that performs metric downward facing odometry which doesn’t depend on triangulation or initialisation, offers observability in an orthogonal direction to a conventional forward facing camera, and is purely a frame-to-frame method. This enables it to be a fast and reliable whilst still being accurate.

In this paper, we pursue the problem of estimating the linear and angular velocity and orientation of a micro aerial vehicle (MAV) equipped with a downward facing camera, an IMU, and a single beam laser rangefinder which measures the height of the vehicle relative to the ground. Broadly, there have been two approaches to tackling visual odometry for downward facing cameras. The first involves exploiting epipolar geometry and using sophisticated structure from motion influenced loosely [2], [3] or tightly coupled visual inertial methods [4], [5]. The other approach makes a planar ground assumption. This enables simple optical flow based velocity estimation where the camera ego motion is compensated for using the angular rate data obtained from a gyroscope, and the velocity is then scaled to metric using some altitude sensor [6]. An issue with all such methods is that their performance is predicated on there being detectable motion between camera frames - the epipolar constraint - which is exacerbated for instance when the camera is nearly static in hovering conditions or moves vertically.

However, if making a planar ground assumption, we can exploit the homography constraint that does not have the aforementioned drawbacks. Implicit means of utilising homography constraints have been presented earlier in appearance based localisation, for instance in [7] where cameras are localised against previously acquired images. Most relevant to our approach, the authors in [8], [9], [10] first estimate the optical flow between features in consecutive frames and then using the aforementioned constraint exploit known angular velocity and ground plane orientation to obtain unscaled velocity. An extended Kalman filter (EKF) is then used to fuse the data and output metric velocity.

In our approach, instead of using sparse visual features, that are dependent on textured environments, we utilise a dense, direct method that makes use of all the visual information present in the camera image, and couple it with angular constraints provided by an IMU within a least squares optimisation.

Contributions of this work include:

- A homography based frame-to-frame velocity estimation algorithm, that is accurate and robust in a wide variety of scenes.
- An EKF structure to incorporate this with a single beam laser rangefinder signal and estimate IMU bias
- Extensive evaluation on a wide variety of environments with comparisons with state of the art algorithms.
### III. Estimation Theory

In this section we present the homography constraint, our optimisation strategy, and the framework to incorporate the corresponding cost functions.

#### A. Homography Constraint and Parameterisation

When looking at points lying on the same plane, their projected coordinates in two images (\(X\) and \(X'\) respectively) taken by a downward camera can be related by

\[
X \equiv HX'
\]

where

\[
H = K(R + t_0/d \cdot n^T)K^{-1} = K(R + t \cdot n^T)K^{-1}
\]

where \(X = [x, y, 1]^T\) and \(X' = [x', y', 1]^T\) are the pixel locations in previous and current image respectively, \(H\) is the warp matrix, \(R\) and \(t\) are the rotation matrix and translation vector from the second camera frame to the previous frame, \(t\) is the unscaled translation, \(n\) and \(d\) are the unit normal vector and distance to the ground plane in second camera frame, and \(K\) is the camera intrinsic matrix (assume known).

During optimisation we parameterise \(R\) as a Rodrigues vector \(r = [r_x, r_y, r_z]^T\) and \(n\) as \(n = [n_x, n_y, n_z]^T\).

\[
\theta = \tan^{-1}(n_y/n_x) \quad \phi = \sin^{-1}(n_z)
\]

Since the IMU provides reliable orientation information, i.e. an estimate of \(R\) and \(n\), three parameterisations are possible: \(p = [t_x, t_y, t_z]^T\), \(p = [t_x, t_y, t_z, r_x, r_y, r_z]^T\) for \(R\) and \(n\) respectively. These parameterisations directly encode the motion of the camera and can easily be initialised using IMU.

#### B. Homography Estimation Cost Function

The parameters of the warp matrix \(H\) are estimated by minimising the SSD error between image pixel intensities. However, a purely photometric cost minimisation may provide incorrect camera pose estimates due to a lack of observability or in the event of non planar objects in the camera field of view. Since the IMU provides reliable orientation information, we add a penalty term which biases the homography solution and avoids these local minima.

Suppose \(X = T(X'; p)\) stands for the homography mapping parameterised by the vector \(p\), we have

\[
p = \arg\min_p \{f_{\text{photo}} + f_{\text{imu}}\}
\]

\[
f_{\text{photo}} = \sum_{j=1}^{N} \|I(T(X_j'; p)) - I'(X_j')\|^2
\]

\[
f_{\text{imu}} = (p - p_0)^T W (p - p_0)
\]

where \(p_0\) is the initial guess obtained from IMU, \(W\) is a diagonal penalty weight matrix, \(I\) and \(I'\) are the previous and current image respectively, and \(X_j'\) is a pixel position in the evaluation region of current image.

#### C. Gauss-Newton Optimisation

We solve for the optimal parameters using iterative Gauss-Newton optimisation. After concatenating all the intensity values of pixel \(X_j'\) in a vector, the Taylor expansion is

\[
f(p + \Delta p) = \|i(p) + G\Delta p - i'\|^2 + (p + \Delta p - p_0)^T W (p + \Delta p - p_0)
\]

where \(i(p) = [I(T(X_j'; p)), \ldots, I(T(X_{N'}; p))]^T\) and \(i' = [I'(X_1'), \ldots, I'(X_{N'}')]^T\). The iterative update to the parameter vector ends up being

\[
\Delta p = (G^T G + W)^{-1} (G^T (i' - i(p)) + W(p_0 - p))
\]

where \(G\) is the jacobian of the photometric residual term. Note that as an optimisation we only choose pixels with a high gradient magnitude similar to [12]. This significantly speeds up computation of the update with negligible loss in accuracy. The detailed timing performance is discussed in Sec. V.

### IV. Visual Inertial Fusion

The optimisation in the previous section outputs an unscaled translation. Inspired by [9], we use an EKF to scale it to metric and additionally filter the frame-to-frame noise.

#### A. Definition

In the following section the superscripts and subscripts \(C\) and \(I\) imply a quantity in frame of the camera and IMU, respectively. The state vector contains camera velocity in the camera frame \(C\), distance to the plane from the camera \(d\), and the linear acceleration in the IMU frame \(I\).

\[
x = [C^T v, d, I^T b]^T, \quad C^T v, I^T b \in \mathbb{R}^3, d \in \mathbb{R}
\]

#### B. Prediction

The derivative of \(C^T v\) can be modeled [9] as

\[
C^T \dot{v} = CR_I \left( l^T a + [l^T \omega]_x I^T p_{IC} + [l^T \omega_m]_x I^T p_{IC} \right) - [C^T \omega_m]_x C^T v
\]

\[
\approx CR_I \left( l^T f_m + l^T g + [l^T \omega_m]_x I^T p_{IC} \right) - [C^T \omega_m]_x C^T v
\]

where \(C \dot{R}_I\) is the rotation matrix from IMU frame to camera frame, \(l^T a\) and \(l^T g\) are the acceleration and gravity in the IMU frame, \(l^T f_m\) and \(l^T \omega_m\) are the raw linear acceleration and angular velocity measured by the IMU (subscript \(m\) denotes raw measurement), and \(C \omega\) is the angular velocity in the camera frame. The subscript \(\times\) denotes the skew symmetric matrix of the vector inside the bracket.

Therefore, the prediction process in discrete EKF can be written as

\[
C^T \dot{v}[k] = C^T \dot{v}[k-1] + \tau C^T \ddot{v}[k]
\]

\[
d[k-1] = d[k-1] + \tau C^T \ddot{v}[k] C n[k]
\]

\[
l^T \dot{b}[k] = l^T \dot{b}[k-1]
\]
Calculating the Kalman gain
and the predicted measurement based on
are available for update, the measurement vector
z
is
updated as
\[
\Sigma[k]_{k-1} = G \Sigma[k] G^T + V \begin{bmatrix}
\text{cov}(f_m) & 0_{3 \times 3} \\
0_{3 \times 3} & \text{cov}(\omega_m)
\end{bmatrix} V^T
\]
(12)

where
\[
G = \frac{\partial \hat{x}[k-1]}{\partial \hat{x}[k-1]} = \begin{bmatrix}
I_3 - \tau^T C_n & 0_{3 \times 3} \\
\tau C_n^T & 0_{3 \times 1}
\end{bmatrix} \in \mathbb{R}^{7 \times 7}
\]
(13)

\[
V = \begin{bmatrix}
\frac{\partial \hat{x}[k-1]}{\partial f_m} & \frac{\partial \hat{x}[k-1]}{\partial \omega_m}
\end{bmatrix} = \begin{bmatrix}
\tau C R_f & \tau (C R_f M + [C v]_x C R_f) \\
0_{1 \times 3} & 0_{1 \times 3} \\
0_{3 \times 3} & 0_{3 \times 3}
\end{bmatrix} \in \mathbb{R}^{7 \times 6}
\]
(14)

\[
M = \begin{bmatrix}
I_{\omega_m}^T & J_{IC}^T \\
0_{3 \times 3} & 0_{3 \times 3}
\end{bmatrix} I_3 + \begin{bmatrix}
\omega_m & I_{IC}^T - 2 I_{IC} \omega_m^T
\end{bmatrix}
\]
(15)

C. Update

When both unscaled velocity and range sensor signal l_m[k]
are available for update, the measurement vector z_m[k]
is
\[
z_m[k] = \begin{bmatrix}
f_m[k] \\
l_m[k] n_{z_m[k]}
\end{bmatrix}
\]
(16)

and the predicted measurement based on \hat{x}[k-1] is
\[
\hat{z}[k-1] = \begin{bmatrix}
C v([k]_{k-1})/d([k]_{k-1}) \\
\hat{d}([k]_{k-1})
\end{bmatrix}
\]
(17)

Calculating the Kalman gain K[k] \in \mathbb{R}^{7 \times 4}
\[
K[k] = \Sigma[k] G^T (J \Sigma[k] G^T + \text{cov}(z_m))^T
\]
(18)

\[
J = \begin{bmatrix}
\hat{x}[k-1] & \hat{d}([k]_{k-1})
\end{bmatrix} \in \mathbb{R}^{4 \times 7}
\]
(19)

Estimates \hat{x}[k] and \Sigma[k] are updated accordingly as
\[
\hat{x}[k] = \hat{x}[k-1] + K[k] (z_m[k] - \hat{z}[k-1])
\]
(20)

\[
\Sigma[k] = (I_7 - K J) \Sigma[k]_{k-1}
\]
(21)

V. Evaluation

We evaluate the performance of our approach on a wide
variety of scenarios and compare and contrast performance
with state of the art algorithms, both in simulation, and with
a real aerial platform. We first present experimental setup
and results in simulation followed by those with real-world
data.

A. Benchmarks and Metrics

Our method (RaD-VIO) is compared to the tracker pro-
aposed in [10] (Baseline), for which we implement the optical
flow method described in [8] and, for fair comparison, use
the same EKF fusion methodology as our approach. Addi-
tionally, we also compare with a state-of-the-art monocular
visual-inertial tracker VINS-Mono [5] without loop closure
(VINS-D, VINS-downward). For additional comparison we
also record the performance of the VINS-Mono tracker on a
forward facing camera (VINS-F), but note that due to very
low overlap between the forward and downward images there
is no correlation between the performance of VINS-D and
VINS-F.

The metrics used are Relative Pose Error (RPE) (the
interval is set to 1s) and Absolute Trajectory Error (ATE) [13].
For ATE, we only report results in the xy plane since the
altitude is directly observed by the rangefinder. We also
report the number of times frame-to-frame tracking fails in
Fig. 4. Since RaD-VIO and Baseline output velocity, the
position is calculated using dead-reckoning. Since a lot of
our trajectories are not closed loops, instead of reporting
ATE we divide it by the cumulative length of the trajectory
(computed at 1s intervals) in the horizontal plane to get the
relative ATE.

B. Simulation Experiments

We utilise AirSim [14], a photorealistic simulator for aero-
vehicles for the purpose of evaluation. The camera generates
240 \times 320 images at a frame rate of 80 Hz. The focal length
is set to 300 pixels. The IMU and the single beam laser
rangefinder output data at 200 Hz and 80 Hz respectively,
and no noises are added.

1) Simulation Test Cases: For the tracking system to
work, the following assumptions or conditions should be met
or partly met:
- The ground should be planar (homography constraint)
- It should be horizontal (parameterisation choice)
- The scene should be static (constancy of brightness)
- Small inter-frame displacement (applicability of warp).

Therefore, the following ten test scenarios are designed to
evaluate the algorithms:
- p1: All assumptions met - ideal conditions
- p2: Viewing planar ground with low texture
- p3: Viewing planar ground with almost no texture
- p4: Viewing planar ground with moving features
- p5: Vehicle undergoing extreme motion
- p6: Camera operating at low frame rate
- s1: Viewing a sloped or a curved surface
- m1: Viewing a plane with small clutter
- m2: Viewing moving features with small clutter
- c1: Viewing a plane with large amounts of clutter

Each of these cases are tested in diverse environments
including indoors, road, and woods. We use 42 data sets in
total for evaluation. Fig. 2 shows some typical images from
these datasets.
2) **Simulation Results and Discussion:** The RPE and relative ATE of all test cases are shown in Fig. 3. For relative ATE our method outperforms both Baseline and VINS-D in almost all the test cases. The velocity error in Fig. 3 (c) contains both velocity bias and random error, and compared to VINS-D our method generates similar velocity errors when the planar assumption is satisfied, but larger when it is not. This error is much smaller than Baseline. Due to the ill-posed nature of the motion and the data in these environments for the forward facing camera, VINS-F performs very poorly.

VINS-D takes a lot of time to initialise the system, and doesn’t do well right after initialisation. During the test, VINS-D occasionally outputs extremely wrong tracking results, and it has difficulty in initialising/re-initialising through quite a few test cases (for instance s1, where although there are enough features on the ground the lighting is challenging). In contrast our tracker never generates any extreme results due to implicitly being constrained by the frame-to-frame displacement.

The simulation shows that RaD-VIO is overall more accurate than compared to Baseline, and when all the assumptions are met, it is slightly more accurate than VINS-D. The test cases demonstrate that the proposed tracker is robust to a lot of non-ideal conditions.

### C. Real-world Experiments

1) **Setup and Test Cases:** To verify the real-world performance of our proposed approach, indoor and outdoor data were collected. The indoor data was obtained from a custom hexrotor platform in a motion capture arena. We use a MatrixVision BlueFox camera configured to output $376 \times 240$ resolution images at a frame rate of 60 Hz, and a wide angle lens with a focal length of 158 pixels. The frame rates of the TeraRanger One rangefinder and the VN-100 IMU are 300 Hz and 200 Hz respectively. The standard deviation of IMU angular velocity and linear acceleration are 0.02 rad/s and 1 m/s² respectively. The indoor ground truth is provided by motion capture system. For outdoor data, only GPS data is provided as a reference, and we use an Intel Aero Drone for data collection. The same algorithm parameters were used as in the simulation experiments for the vision and optimisation frontends, and the parameters for the EKF were tuned based on the sensor noise for the respective configuration.

2) **Experiment Results and Discussion:** The tracking errors are shown in Fig. 7. Similar to the simulation results for relative ATE our tracker is on average better than both Baseline and VINS-D. As for the translation part of RPE, our method is always better or no worse than the other two methods except for the last case in p4 (moving features) and p5 (extreme motion). In these cases the robust sparse feature selection in VINS-D avoids being overly influenced. RaD-VIO is not as robust to extreme motion as it is in simulation, and there are two reasons: the IMU input is more noisy and the wider field of view ends up capturing objects outside the ground plane that adversely affect the alignment. For

![Fig. 3: Comparison of the algorithms on the simulation datasets described in Sec. V-B.1.](image)

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https://www.intel.com/content/www/us/en/products/drones/aero-ready-to-fly.html
Fig. 4: Percentage of tracking failures: The failure instances of Baseline and RaD-VIO are calculated by a per-frame counter, while that of VINS-D is estimated according to gap between messages, not including time taken for initialisation.

Fig. 5: Comparison of algorithms in simulation for a figure 8 trajectory. Rotation part of RPE, both Baseline and RaD-VIO are better than VINS-D; this is because both the latter two approaches use the IMU rotation directly.

The figure 8 trajectory and velocity of an outdoor test is shown in Fig. 10.

The experiment results show that the proposed method is able to work well in real world even in the presence of sensor synchronisation issues and large noises in the IMU signal.

D. Timing Benchmarks

We evaluated the tracking framerate of RaD-VIO on a desktop PC with an Intel i7-6700K CPU. The frame rate of the tracker is on average 150Hz over all of our datasets. As can be seen Table II bags with less features and large inter-frame displacements result in lower frame rate due to longer time required for convergence.

VI. CONCLUSIONS AND FUTURE WORK

We present a framework to obtain 6 degree of freedom state estimation on MAVs using a downward camera, IMU, downward single beam laser range finder. The proposed approach first extracts the rotation and unscaled translation between two consecutive image frames based on a cost function that combines dense photometric homography alignment and a rotation prior from the IMU then uses an EKF to perform sensor fusion and output a filtered metric linear velocity.

Extensive experiments in a wide variety of scenarios in simulations and in real-world experiments demonstrate the
Fig. 8: RPE and ATE of tested simulation bag files: The circle marker means the data point is not reliable due to a large number of tracking failures. The errors drawn at the upper boundary are clipped.

Fig. 9: Comparison of algorithms in a real-world indoors dataset with motion capture ground truth. Accuracy and robustness of the tracker under extenuating circumstances. The performance exceeds the frame-to-frame tracking framework proposed in [8], [10], and is slightly better than a current state of the art monocular visual-inertial odometry algorithm. Further advantages of the proposed tracker are that it is stable and never generates extremely diverged state estimates (as triangulation based optimisation methods are susceptible to), and can operate at a high frame rate. A qualitative comparison of the performance on simulation data is shown in Table II.

For future work, in line with our introductory statements, we intend to couple the performance of such a downward facing tracker with a conventional sliding window optimisation based tracker to develop a resilient robotic system that exploits the individual strengths of both odometry approaches.

| Category                      | Mean  | σ     | Min  | Max  |
|-------------------------------|-------|-------|------|------|
| Stable case                   | 159   | 11.9  | 123  | 181  |
| Less or no feature (p2, p3)   | 143   | 12.4  | 125  | 160  |
| Large transform (p5, p6)      | 139   | 17.8  | 107  | 159  |
| All                           | 153   | 15.7  | 107  | 181  |

Table I: Tracker Frame Rate Evaluation

| Conditions               | Baseline | RaD-VIO | VINS-D |
|--------------------------|----------|---------|--------|
| Ideal (p1)               | ++       | +++     | +++    |
| Low texture (p2)         | +        | +++     | +++    |
| Negligible texture (p3)  | not work | +++     | +      |
| Moving features (p4, m2) | -        | -       | ++     |
| Extreme motion (p5)      | -        | +++     | +++    |
| Low image Hz (p6)        | -        | +++     | ++     |
| Slope (s1)               | +++      | +++     | ++     |
| Medium clutter (m1)      | +        | ++      | +++    |
| High clutter (c1)        | +        | +       | +++    |

+++: Low or no tracking failures, ++: Occasional failures, +: Frequent failures, -: Works poorly, *: slightly better than VINS-D

Table II: Qualitative Performance Comparison on Simulation Data
REFERENCES

[1] J. Delmerico and D. Scaramuzza, “A benchmark comparison of monocular visual-inertial odometry algorithms for flying robots,” in IEEE International Conference on Robotics and Automation (ICRA), no. CONF, 2018.

[2] S. Weiss, M. W. Achtelik, S. Lynen, M. Chli, and R. Siegwart, “Real-time onboard visual-inertial state estimation and self-calibration of mavs in unknown environments,” in Robotics and Automation (ICRA), 2012 IEEE International Conference on. IEEE, 2012, pp. 957–964.

[3] C. Forster, Z. Zhang, M. Gassner, M. Werlberger, and D. Scaramuzza, “Svo: Semidirect visual odometry for monocular and multicamera systems,” IEEE Transactions on Robotics, vol. 33, no. 2, pp. 249–265, 2017.

[4] A. I. Mourikis and S. I. Roumeliotis, “A multi-state constraint kalman filter for vision-aided inertial navigation,” in Robotics and automation, 2007 IEEE international conference on. IEEE, 2007, pp. 3565–3572.

[5] T. Qin, P. Li, and S. Shen, “Vins-mono: A robust and versatile monocular visual-inertial state estimator,” IEEE Transactions on Robotics, no. 99, pp. 1–17, 2018.

[6] D. Honegger, L. Meier, P. Tanskanen, and M. Pollefeys, “An open source and open hardware embedded metric optical flow cmos camera for indoor and outdoor applications,” in Robotics and Automation (ICRA), 2013 IEEE International Conference on. IEEE, 2013, pp. 1736–1741.

[7] B. Steder, G. Grisetti, C. Stachniss, and W. Burgard, “Visual slam for flying vehicles,” IEEE Transactions on Robotics, vol. 24, no. 5, pp. 1088–1093, 2008.

[8] V. Grabe, H. H. Bülthoff, and P. R. Giordano, “On-board velocity estimation and closed-loop control of a quadrotor uav based on optical flow,” in Robotics and Automation (ICRA), 2012 IEEE International Conference on. IEEE, 2012, pp. 491–497.

[9] V. Grabe, H. H. Bülthoff, and P. R. Giordano, “A comparison of scale estimation schemes for a quadrotor uav based on optical flow and imu measurements,” in Intelligent Robots and Systems (IROS), 2013 IEEE/RSJ International Conference on. IEEE, 2013, pp. 5193–5200.

[10] V. Grabe, H. H. Bülthoff, D. Scaramuzza, and P. R. Giordano, “Nonlinear ego-motion estimation from optical flow for online control of a quadrotor uav,” The International Journal of Robotics Research, vol. 34, no. 8, pp. 1114–1135, 2015.

[11] D. Crispell, J. Mundy, and G. Taubin, “G taubin, parallax-free registration of aerial video,” in in Proceedings of the British Machine Vision Conference (BMVC). Citeseer, 2008.

[12] K. S. Shankar and N. Michael, “Robust direct visual odometry using mutual information,” in 2016 IEEE International Symposium on Safety, Security, and Rescue Robotics (SSRR). IEEE, 2016.

[13] R. Kümerle, B. Steder, C. Dornhege, M. Ruhnke, G. Grisetti, C. Stachniss, and A. Kleiner, “On measuring the accuracy of slam algorithms,” Autonomous Robots, vol. 27, no. 4, p. 387, 2009.

[14] S. Shah, D. Dey, C. Lovett, and A. Kapoor, “Airsim: High-fidelity visual and physical simulation for autonomous vehicles,” in Field and Service Robotics, 2017. [Online]. Available: https://arxiv.org/abs/1705.05065