1. Introduction

Lithium-ion batteries (LIBs) have been extensively applied in portable electronics and are expected to be used in electric vehicles (EV) and plug-in hybrid electric vehicles (HEV). Further improvements in energy and power density put forward higher requirements on either new electrode materials or their novel structural design. In the past few decades, significant efforts have been made to meet these needs. Rutile SnO2 has become one of the most promising substitutes for graphite anode materials owing to its high theoretical capacity (781 mAh g\(^{-1}\)) compared to the theoretical capacity (372 mAh g\(^{-1}\)) of graphite.\(^1\)\(^-\)\(^4\) However, there is a severe impediment to the development of SnO2 as anode materials for LIBs because of its poor electric conductivity. Moreover, compared with two-dimensional materials, such as black phosphorus (BP), defective graphene, Li diffusion energy barrier in the bulk SnO2 is high.\(^5\)\(^-\)\(^7\) Therefore, it is necessary to find a feasible method to improve electronic and ionic conductivities of SnO2.

The conduction property of SnO2-based composites with conducting materials (such as carbonaceous materials and conducting polymers) is high in comparison with SnO2, in accordance with the quantitative experiments.\(^8\)\(^-\)\(^11\) Meanwhile, other methods used to improve the rate property of SnO2 also play an essential role. For instance, doping, the metal cationic (such as Al, Mo, Ni, Co, Cu, Sb, W) doping, non-metal anionic (such as N, P, F) doping, or metal and non-metal (such as Ni–N, Co–N, Cu–N) co-doping can also be used to enhance the electrochemical properties of SnO2 as anode materials.\(^12\)\(^-\)\(^22\) Moreover, the rate property of SnO2 with graphene as electrode for LIBs was investigated by Miao et al. based on the density functional theory (DFT) method.\(^6\) They found that the Li ionic conductivity of SnO2 with graphene was enhanced due to a new Li diffusion path [110] with a low diffusion barrier of Li compared to the pristine SnO2 with [001] direction.\(^6\)\(^7\)

Although the electronic and ionic conductivities of SnO2 as the anode material for LIBs can be enhanced with distinguishable modified techniques. However, the improvement of SnO2 by doping with impurity atoms mainly focuses on the experiment. There are few investigations to explain why the rate property of SnO2 improved by doping is high compared with the pure SnO2. Therefore, herein, the electronic and ionic conductivities of SnO2 as anode materials for LIBs were calculated using the DFT method, and the effects of doping atoms (Ni or Ni-N) on electronic and ionic conductivities of SnO2 were investigated.

2. Simulation methodology

The DFT calculations were performed using the SIESTA (Spanish Initiative for Electronic Simulations with Thousands of Atoms) with Perdew–Burke–Ernzerhof (PBE) generalized
So, it is important to first investigate the stability of SnO₂ in order to explore the possibility of its synthesis. We use the formation energy descriptor to measure the stability of doped SnO₂. The calculated formation energies of Ni doping and Ni–N co-doping 2.21 eV and 2.70 eV, respectively. Low formation energies of defects generally mean that these defects form easily. The result indicates that Ni-doped SnO₂ and Ni–N co-doped SnO₂ are energetically favorable, which is consistent with the experimental observations.

The conduction property of SnO₂ by doping (Ni, Ni–N co-doping) was investigated by considering their electronic structures calculated based on the DFT. The calculated band structure and density of states (DOS) of the bulk SnO₂ are shown in Fig. 2 (a) and (b), respectively. It is shown that the bulk SnO₂ is a semiconductor with a direct band gap of 2.08 eV. Its band gap is within other calculations (1.6 to 2.3 eV), as shown in Fig. 2 (a), where the Fermi level is zero. Fig. 2(b) shows that the energy states near the Fermi level (E_f) are mainly occupied by electrons in the 2p orbital of O atoms. The conduction band is largely contributed by 5s states of Sn atom. However, the band gaps of Ni-doped and Ni–N co-doped SnO₂ are 1.07 eV and 0.94 eV, respectively, as shown in Fig. 3(a) and (c), which both are smaller about 1 eV than that of the bulk SnO₂. Therefore, the partial transfer of electrons caused by thermal excitation from the valence band to conduction band will be more effortless in the doped SnO₂ than in the pure SnO₂.

Moreover, it can be seen from Fig. 3(b) that the E_f is localized at the maximum of the valence band (VBM) for Ni-doped SnO₂, as well as the states near E_f mainly consist of 3d states of Ni atom. For Ni–N co-doped SnO₂, as shown in Fig. 3(d), the states near E_f are occupied primarily by 3d states of Ni and 2p states of N. This indicates that the states near E_f can be changed by doped atoms (Ni, Ni–N) for the bulk SnO₂ to improve their electronic structures. Then their degree of conductivity has been enhanced by doping with Ni and Ni–N. In addition, the conductivity of Ni–N co-doped SnO₂ is a little better than that of Ni-doped SnO₂ according to their energy gaps. The Li ion property of SnO₂ as anode material for LIBs is as significant as its electronic property discussed above. Therefore, the following Li diffusion properties of SnO₂ and SnO₂ doped were studied in the light of Li diffusion energy barrier calculated with the DFT.

### 3. Results and discussion

The nearest neighboring heteroatom doping was only considered in our work. According to the symmetry of SnO₂, each Sn atom has 8 the nearest neighboring Sn atoms and 6 the neighboring O atoms, respectively, as shown in Fig. 1. Therefore, one Ni position doping and one Ni–N position co-doping were studied. Consider first, some materials demonstrate good computational performance but are difficult to synthesize, which limits their application in experiments or in practice.

#### Table 1 Lattice parameters of the rutile SnO₂

|   | a (Å) | b (Å) | c (Å) | Ref. |
|---|---|---|---|---|
| Cal. | 4.734 | 3.220 | 7 |
| Exp. | 4.737 | 3.186 | 25 |
| Ours | 4.85 | 3.29 | (PBE) |

The crystal structure of the bulk SnO₂, where the big and small balls are Sn and O atoms, respectively. The relaxation of the pristine SnO₂ unit cell was performed with a conjugate gradient (CG) method until the maximum force was less than 0.02 eV Å⁻¹. The optimized bulk structure is shown in Fig. 1, where big and small balls are Sn and O atoms, respectively. The calculated bulk equilibrium lattice constant of SnO₂ is \(a = b = 4.85\) Å, \(c = 3.29\) Å, which is almost identical to the experimental and calculational values, as listed in Table 1. A Ni occupies a Sn site (Ni-doping) and a Ni occupies a Sn site while a N replaces a O site (Ni–N co-doping) in \(2 \times 2 \times 3\) SnO₂ supercells were used to study. A \(1 \times 1 \times 3\) k-point mesh to relax the Ni-doped SnO₂ and Ni–N co-doped SnO₂. The Li diffusion barrier and band structure were computed after relaxing.

#### Fig. 2 (a) and (b) are the band structure and the density state of the bulk SnO₂, respectively. The dashed black line is the Fermi level that its value is zero.
method. The diffusion energy barrier of Li in the bulk SnO₂ obtained is 0.24 eV, as shown in Fig. 4(a). Moreover, the diffusion path (a path from A point to D point) shown in Fig. 4(b), is identical to the experimental observation that Li diffusion direction is dominated by the [001] direction,⁶,⁷ which both is a one-dimensional diffusion path.

The diffusion path of Li in Ni-doped SnO₂ and Ni–N co-doped SnO₂ remains one-dimensional, as shown in Fig. 5(b) and (c), but the diffusion energy is different. It can be seen from Fig. 5(a) that the energy barriers of Li for the nearest neighbor diffusion path (from B to C point) in the Ni-doped SnO₂ and Ni–N co-doped SnO₂ are 0.02 eV and 0.12 eV, which are both less than the value (0.24 eV) of the bulk SnO₂, which exhibits that the Li ionic conductivity of Ni-doped SnO₂ and Ni–N co-doped SnO₂ has been greatly improved for the nearest neighbor path. Furthermore, the energy barriers of Li far from the nearest-neighbor diffusion path (such as from C to D point, D to E point, and E to F point) be also calculated to see the effect of dopant atoms on all diffusion properties. For Ni-doped SnO₂, diffusion barriers of Li from C to D, D to E site, and E to F position, are 0.57 eV, 0.25 eV and 0.24 eV, respectively. The Li diffusion for the second nearest neighbor Li (from C to D site) is more difficult in Ni-doped SnO₂ than in the pure SnO₂. The adsorption energies of Li at C position for pure SnO₂, Ni-doped SnO₂ and Ni–N co-doped SnO₂ are −1.28 eV, −3.52 eV and −2.56 eV, respectively. The results show that lithium is energetically able to adsorb on C site for Ni-doped SnO₂, and Li diffusion barrier (from C to D site) as shown in Fig. 5(a) would increase because of a strong Li adsorption. Above results indicates that although the electronic conductivity of SnO₂ can be improved by Ni doping, the ionic conductivity was reduced when one Sn atom was replaced by one Ni atom because of a stronger Li adsorption at C site for Ni-doped SnO₂. Therefore, it is not beneficial to improve the electrochemical properties of SnO₂ as anode material for LIBs. However, for Ni–N co-doped SnO₂, the diffusion energy of Li from C to D position is 0.22 eV. It almost is the same as that of the pure SnO₂. Meanwhile, the energy barriers of Li (from B to C) just described above in the Ni–N co-doped SnO₂ are 0.12 eV.

The ionic conductivity of SnO₂ was enhanced by Ni–N co-doping. Therefore, both the electronic and ionic conductivity
of SnO₂ can be improved by Ni–N co-doping. It illustrates that Ni–N co-doping in the pure SnO₂ is energetically favorable to promote the rate performance of SnO₂.

4. Conclusions

In conclusion, Ni–N co-doping in the pure SnO₂ is energetically favorable to improve both the electronic and ionic conductivity. The results calculated that the band gaps of Ni-doped and Ni–N co-doped SnO₂ are 1.07 eV and 0.94 eV, which both are smaller than the value 0.24 eV of the pure SnO₂. The diffusion energy barrier of Li from C to D for Ni-doped SnO₂ is 0.57 eV larger than the value 0.24 eV for SnO₂. However, the diffusion energy barrier of Li from B to C for Ni–N co-doped SnO₂ is 0.12 eV smaller than the value 0.24 eV for SnO₂. Meanwhile, the diffusion energy barriers of Li along pathways far from the nearest neighbor path for Ni–N co-doped SnO₂ is almost the same as 0.24 eV for SnO₂. Our results demonstrate that the electronic and ionic conductivity of SnO₂ can be promoted by Ni–N co-doping, and provides a theoretical explanation to enhance the rate property of SnO₂ by Ni–N co-doping.

Conflicts of interest

There are no conflicts to declare.

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