New results on inclusive $B \rightarrow X_u \ell \nu$ decay from the Belle experiment

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We report on the measurement of inclusive charmless semileptonic $B$ decays $B \rightarrow X_u \ell \nu$. The analysis makes use of hadronic tagging and is performed on the full data set of the Belle experiment comprising 772 million $B\bar{B}$ pairs. In the proceedings, the preliminary results of measurements of partial branching fractions and the CKM matrix element $|V_{ub}|$ are presented.
1. Introduction

In the Standard Model of particle physics (SM), the Cabibbo-Kobayashi-Maskawa (CKM) matrix [1, 2] describes the quark mixing and accounts for CP-violation in the quark sector. One of the crucial tests of the SM is precise determination of the magnitude of the matrix elements. In the flavor scope, the corresponding world averages of $|V_{ub}|$ from both exclusive and inclusive determinations [3] are

$$|V_{ub}^{\text{excl.}}| = (3.67 \pm 0.09 \pm 0.12) \times 10^{-3},$$

$$|V_{ub}^{\text{incl.}}| = (4.32 \pm 0.12 \pm 0.13) \times 10^{-3},$$

where the uncertainties are from experiment and theory. The disagreement between them is about three standard deviations.

On the other hand, the experimental measurement of the inclusive semileptonic decay $B \to X_u \ell \nu$ is challenging due to the large background from the CKM-favoured $B \to X_c \ell \nu$ decay. Fig. 1 illustrates the $B \to X_u \ell \nu$ and $B \to X_c \ell \nu$ decays with the generator-level distributions in two important kinematic variables: the invariant mass of hadronic system $M_X$ and the lepton energy in the signal $B$ rest frame $E^B_{\ell}$. It’s shown that the clear separation of the signal decay is only possible in certain kinematic regions, e.g. the endpoint of lepton energy or the low $M_X$ region. The details of the reconstruction and separation strategy is described in Sec. 2. The preliminary results on the measured partial branching fractions and the $|V_{ub}|$ values are presented in Sec. 3.

![Figure 1: The generator-level $M_X$ and $E^B_{\ell}$ distributions of the $B \to X_u \ell \nu$ decay comparing to that of $B \to X_c \ell \nu$ decay. The $B \to X_c \ell \nu$ component (gray) is scaled down by a factor of 50 for illustration.](image)

2. Analysis strategy

The data used in this analysis were recorded with the Belle detector [4] at the KEKB accelerator complex [5] with a center-of-mass energy of $\sqrt{s} = 10.58$ GeV. The full data set contains an integrated luminosity of 711 fb$^{-1}$ and corresponds to 772 million $\Upsilon(4S) \to B\bar{B}$ events. The Monte Carlo (MC) simulated events are generated by EVTGEN [6] and the detector response is modeled using GEANT3 [7]. The signal $B \to X_u \ell \nu$ MC sample is a combination of resonances and non-resonant decay using a hybrid modelling approach [8, 9]. The non-resonant component is based on the theory calculation of Ref. [10] with the model parameters in the Kagan-Neubert scheme from Ref. [11].

The hadronic decays of one of the $B$ mesons are reconstructed via the full reconstruction algorithm [12] based on neural networks. In total, over 1104 decay cascades are considered and
reconstructed. The efficiencies for charged and neutral $B$ mesons are 0.28% and 0.18%, respectively [13]. The output classifier score of this algorithm presents the quality of the reconstructed candidates. We select the best candidate of $B_{\text{tag}}$ for each event. In addition, we require the beam-constrained mass $M_{\text{bc}} = \sqrt{(\sqrt{s}/2)^2 - |p_{\text{tag}}|^2} > 5.27$ GeV to suppress continuum processes ($e^+e^- \rightarrow q\bar{q}$, $q = u, d, s, c$) and beam background.

All tracks and clusters not used in the construction of the $B_{\text{tag}}$ candidate are used to reconstruct the signal side. With the fully reconstructed four-momentum of $B_{\text{tag}}$ and the known beam-momentum, the signal $B$ rest frame can be defined as

$$p_{\text{sig}} = p_{e^+e^-} - \left(\sqrt{m_B^2 + |p_{\text{tag}}|^2}, p_{\text{tag}}\right).$$

The signal lepton with $E_\ell^B = |p_\ell^B| > 1$ GeV is used to identify the semileptonic decays. Here the small correction of the lepton mass term to the energy of the lepton is neglected. A veto on lepton-pair mass is applied to reject the lepton from $J/\psi$ decay and photon conversions. In addition, the charge of lepton is required to be opposite to $B_{\text{tag}}$ for the charged $B$ case. With the signal lepton selected, the four-momentum of hadronic system $p_X$ is defined as a sum of the four-momenta of tracks and clusters which are not involved in reconstructing the $B_{\text{tag}}$ and signal lepton. Furthermore, we reconstruct the missing mass squared and the four-momentum transfer squared $q^2$ as

$$MM^2 = (p_{\text{sig}} - p_X - p_\ell)^2, \quad q^2 = (p_{\text{sig}} - p_X)^2.$$

We utilise a machine learning based classification with boosted decision trees (BDTs) to separate the signal $B \rightarrow X_u\ell\nu$ decay from the background events which are dominated by $B \rightarrow X_c\ell\nu$. The feature variables used for training include $MM^2$, the number of charged kaons and $K_S^0$, the total charge of event, the vertex fit $\chi^2$/dof between the hadronic system and signal lepton, and the $MM^2$ and angular information of a partially reconstructed $B \rightarrow D^*\ell\nu, D^* \rightarrow D\pi_{\text{slow}}$ decay with the slow pions candidates, where $p_{\pi_{\text{slow}}} < 0.22$ GeV. Due to the small difference between the masses of $D$ and $D^*$, the flight directions of the $\pi_{\text{slow}}$ and $D^*$ are strongly correlated and we estimate the energy of $D^*$ as $E_{D^*} \approx m_D \times E_{\pi_{\text{slow}}}/(m_{D^*} - m_D)$. On the BDT classifier output, we choose a selection criteria that reject 98.1% of $B \rightarrow X_c\ell\nu$ decays and retain 24.8% of $B \rightarrow X_u\ell\nu$ signal decays. The selection efficiency on data is 2.3%.

In addition, the $B_{\text{tag}}$ reconstruction efficiency is calibrated using a data-driven approach described in Ref. [14]. The uncertainty of calibration is considered in systematics. We also apply a continuum efficiency correction to the simulated sample by comparing the difference to the number of reconstructed off-resonance events in data.

3. Partial branching fractions and $|V_{ub}|$ results

A binned likelihood fit is performed to extract the signal yield, where the systematic uncertainties are incorporated via nuisance-parameter constraints. The fit uses MC templates for background, and for signal in and out-side of the selected phase-space regions. In total, we carry out five separate fits to measure the three partial branching fractions as summarised in Table 1. Fig. 2 shows the main fit results. The result based on the two-dimensional fit of $M_X$ and $q^2$, i.e.
ΔBF = (1.56 ± 0.06 ± 0.12) × 10^{-3}, is in a good agreement with the one obtained by fitting the lepton spectrum, covering the same phase-space region. It also agrees well with the most precise measurement to date of this region [15], where ΔBF = (1.55 ± 0.12) × 10^{-3}. For other phase-space regions, the measured partial branching fractions are also compatible with the previous measurements [16].

Based on the measured partial branching fractions, we calculate the $|V_{ub}|$ value with the theoretical input of decay rate as

$$|V_{ub}| = \sqrt{\frac{\Delta B(B \to X_u \ell \nu)}{\tau_B \Delta \Gamma(B \to X_u \ell \nu)}},$$

(4)

where the average $B$ meson lifetime is taken as (1.579 ± 0.004) ps [17] and the state-of-the-art theory predictions on $\Delta \Gamma$ are listed in Table 2. Table 3 summarises the measured $|V_{ub}|$ values. To quote a single value for $|V_{ub}|$ we adapt the procedure of Ref. [17] and calculate a simple arithmetic

| Fit | Fit variable | Phase-space region | $10^3\Delta B$ |
|-----|--------------|--------------------|----------------|
| (a) | $M_X$        | $E^{B}_\ell > 1$ GeV, $M_X < 1.7$ GeV | 1.04 ± 0.04 ± 0.07 |
| (b) | $q^2$        | $E^{B}_\ell > 1$ GeV, $M_X < 1.7$ GeV, $q^2 > 8$ GeV^2 | 0.70 ± 0.06 ± 0.09 |
| (c1)| $E^{B}_\ell$ | $E^{B}_\ell > 1$ GeV, $M_X < 1.7$ GeV | 1.09 ± 0.05 ± 0.10 |
| (c2)| $E^{B}_\ell$ | $E^{B}_\ell > 1$ GeV | 1.66 ± 0.08 ± 0.17 |
| (d) | $M_X - q^2$  | $E^{B}_\ell > 1$ GeV | 1.56 ± 0.06 ± 0.12 |

Table 1: The measured partial branching fractions for various phase-space regions. The first uncertainty is statistical and the second one is systematics.
average of the most precise determinations for the phase-space region is statistical, the second one is systematic and the last term comes from the corresponding theory calculation.

Table 3: The theory predicted decay rates in the three phase-space regions (ps⁻¹).

| Phase-space region | BLNP [20] | DGE [21, 22] | GGOU [23] | ADFR [24, 25] |
|--------------------|-----------|-------------|-----------|-------------|
| $M_X < 1.7$GeV     | 45.2±5.4  | 42.3±5.8    | 43.7±4.9  | 52.3±5.4    |
| $M_X < 1.7$GeV, $q^2 > 8$GeV² | 23.4±3.4  | 24.3±2.6    | 23.3±3.2  | 31.1±2.6    |
| $E_f^B > 1$GeV     | 61.5±6.4  | 58.3±3.6    | 58.5±2.7  | 61.5±5.8    |

Table 2: The theory predicted decay rates in the three phase-space regions (ps⁻¹).

| Fit | $10^3|V_{ub}|$ | $10^3|V_{ub}|$ | $10^3|V_{ub}|$ | $10^3|V_{ub}|$ |
|-----|----------------|----------------|----------------|----------------|
|     | BLNP           | DGE            | GGOU           | ADFR           |
| (a) | $3.81^{+0.08,+0.13,+0.21}_{-0.08,-0.13,-0.21}$ | $3.99^{+0.08,+0.14,+0.20}_{-0.08,-0.14,-0.26}$ | $3.88^{+0.08,+0.13,+0.15}_{-0.08,-0.14,-0.16}$ | $3.55^{+0.07,+0.12,+0.17}_{-0.07,-0.12,-0.17}$ |
| (b) | $4.35^{+0.18,+0.26,+0.26}_{-0.18,-0.28,-0.28}$ | $4.27^{+0.17,+0.26,+0.18}_{-0.18,-0.28,-0.21}$ | $4.30^{+0.18,+0.27,+0.24}_{-0.18,-0.28,-0.27}$ | $3.77^{+0.15,+0.23,+0.17}_{-0.16,-0.24,-0.17}$ |
| (c1)| $3.90^{+0.09,+0.17,+0.21}_{-0.10,-0.18,-0.21}$ | $4.08^{+0.10,+0.18,+0.20}_{-0.10,-0.19,-0.26}$ | $3.99^{+0.09,+0.18,+0.15}_{-0.10,-0.19,-0.16}$ | $3.63^{+0.09,+0.16,+0.17}_{-0.09,-0.17,-0.17}$ |
| (c2)| $4.14^{+0.10,+0.20,+0.18}_{-0.10,-0.22,-0.20}$ | $4.25^{+0.10,+0.21,+0.11}_{-0.10,-0.22,-0.12}$ | $4.24^{+0.10,+0.21,+0.09}_{-0.10,-0.22,-0.10}$ | $4.14^{+0.10,+0.20,+0.18}_{-0.10,-0.22,-0.18}$ |
| (d) | $4.01^{+0.08,+0.15,+0.18}_{-0.08,-0.16,-0.19}$ | $4.12^{+0.08,+0.16,+0.11}_{-0.09,-0.16,-0.12}$ | $4.11^{+0.08,+0.16,+0.08}_{-0.09,-0.16,-0.09}$ | $4.01^{+0.08,+0.15,+0.18}_{-0.08,-0.16,-0.18}$ |

The value extracted in this analysis is larger but compatible with the value expected from CKM unitarity from a global fit of Ref. [19] of $|V_{ub}| = (3.62^{+0.11}_{-0.08}) \times 10^{-3}$ within 1.6 standard deviations.

4. Summary and outlook

The preliminary results are obtained with the hadronic tagged analysis based on the full Belle data set. The measured partial branching fractions for the three phase-space regions are compatible with the previous measurements. The preliminary $|V_{ub}|$ value extracted in this analysis is larger but compatible with the exclusive determination within 1.4 standard deviations. Based on this preliminary result, the final analysis will incorporate a few modifications, including the aspects of increasing the simulated sample size and considering additional systematics accounting for the signal modeling. The separate-mode branching fractions for $B^+/B^0$ and $\epsilon/\mu$ will be also provided.

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Lu Cao

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