A COMPUTATIONAL VIEW OF THE COGNITIVE SEMANTICS OF SPATIAL PREPOSITIONS

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Abstract
This paper outlines the linguistic semantic commitments underlying an application which automatically constructs depictions of verbal spatial descriptions. Our approach draws on the ideational view of linguistic semantics developed by Ronald Langacker in his theory of Cognitive Grammar, and the conceptual representation of physical objects from the two-level semantics of Bierwisch and Lang. In particular the dimensions of the process of conventional imagery are used as a metric for the design of our own conceptual representation.

INTRODUCTION
An increased interest in the semantics of spatial language has accompanied the recent rise in popularity of cognitive linguistics (see [Rudzka-Ostyn1988]), yet computational approaches are thin on the ground. This can in part be accounted for by the rather descriptive and unformalized nature of the theories developed, but is more likely due to the adoption of an ideational view of linguistic meaning which, it seems, is an anathema to computational linguists. In this paper we take a serious, if informal, look at Ronald Langacker's theory of Cognitive Grammar [Langacker1987], [Langacker1988a], [Langacker1988b], more specifically its commitment to conceptualization and the use of conventional imagery.

The first section of this paper introduces the semantics of projective prepositions (eg. "in front of", "behind", "left of", "right of"), illustrating that these seemingly simple predicates are surprisingly complex and ambiguous. In the light of this discovery the following sections consider Langacker's view of linguistic meaning, and the design of a conceptual representation for spatial prepositions motivated by the consideration of the various dimensions of conventional imagery. The representation has been implemented for English spatial descriptions and after demonstrating its utility for the automatic depiction of verbal descriptions, we finally contrast our approach against previous attempts.

THE SEMANTICS OF PROJECTIVE PREPOSITIONS
In this section we characterize the components of the spatial meaning of projective prepositions that have motivated our interest in cognitive linguistic approaches. Throughout, the decoding problem, that is, generating adequate meanings for a locative expression in a particular situation, is our benchmark for representational adequacy.

The spatial meaning of a projective prepositional predication (eg. "the chair is in front of the desk") can include: a constraint on the proximity of the located (LO) (eg. "the chair") and reference objects (RO) (eg. "the desk"); a directional constraint on the LO relative to the RO; and a relative orientation between the speaker, LO and RO. Constraints are of an intrinsically fuzzy nature such that different relative positions and orientations of the speaker, RO and LO satisfy the predication to different degrees, and combinations of constraints on the RO and LO originating from different predications must be readily accommodated.

PROXIMITY CONSTRAINTS
Projective prepositions necessarily place a constraint on the proximity of the located object and the reference object. Predications such as "the chair is in front of the desk" constrain the "desk" and "chair", to some degree, to be proximal to each other. Conversely projective prepositions such as "away from" predicate a distal relationship between the located and reference object. The degree of the proximity expressed in any projective prepositional predication varies accord-
INTUITIVE. In the intrinsic case the reference frame is centered at the RO and adopts the intrinsic orientations of the RO. Thus a LO is deemed to be “in front of” the RO under an intrinsic reading if it is located in the direction defined by the vector that is the half-plane of the front of the RO. In figure 1 stool number 1 is intrinsically “in front of the desk”.

DEICTIC The reference frame for a deictic interpretation is centered at the speaker and adopts the speaker’s orientation; deictic readings can be invoked explicitly with qualifications such as “from where we are standing”; when the RO has no intrinsic or extrinsic sideness relating to the preposition used; or when intrinsic or extrinsic interpretations are ruled out on other grounds (eg. the impossibility of spatially arranging the objects as required by the interpretation). In figure 1 stool number 2 is deictically “in front of the desk”.

EXTRINSIC Extrinsic readings can occur when the RO has no intrinsic sides relating to the locative preposition (eg. for objects such as trees) but is in close proximity to another object that is strongly sided (eg. such as a house); in which case the reference frame capturing the intrinsic orientations of the stronger sided object can be adopted by the RO. Referring to figure 1 the chair is extrinsically “in front of stool number 3”; here the stool has inherited an extrinsic front from the right wall.

INTERACTING CONSTRAINTS
Typically an object is located with respect to more than one RO by the means of multiple spatial predications. This places a requirement of on the meaning representation of spatial predications that they must capable of being easily combined, to give rise to a cumulative meaning.

COGNITIVE GRAMMAR AND LINGUISTIC MEANING
Cognitive grammar is comprised of five basic claims as to the composition of linguistic meaning, following [Langacker1988b] these are:

1. Meaning reduces to conceptualization.
2. Polysemy is the norm and can be adequately accommodated by representing the meaning a lexical item as a network of senses related by categorizing relationships of schematicity or extension.
3. Semantic structures are characterized relative to cognitive domains. Domains are hierarchically
organized in terms of conceptual complexity, where the characterization of a concept at one level can draw on lower level concepts. While there need not necessarily be any conceptual primitives, the lowest level domains are termed basic domains and include our experience of time, space, color etc.  

4. A semantic structure derives its value through the imposition of a "profile" upon a "base".  

5. Semantic structures incorporate conventional "imagery", our ability to construe the same informational content in different ways.  

That meaning reduces to conceptualization (thesis 1), is characterized relative to cognitive domains (thesis 3), and incorporates conventional imagery (thesis 5) runs in stark contrast to the heavy emphasis placed on truth conditions and formalization by current computational linguistic approaches. We have attempted to tackle the informality of this ideational view of meaning, by addressing one particular basic cognitive domain, that of oriented three-dimensional space, and implement a restricted version of Langacker's process of conceptualization by means of conventional imagery. To verify the utility of the resulting conceptualualization, we use the interpretations of spatial expressions so generated (the resulting images), to automatically construct a depictions of the scene.  

Theses 2, that prototypes should replace traditional objective categories, lies at the very heart of cognitive semantics [Taylor1989], and though it is widely accepted as true for semantic and most other linguistic categories, prototype theory is not conducive to rigorous formalization and has consequently been ignored by mainstream computational linguistics. Likewise our concern is with meaning variations that originate from different construals of the same information in the process of conventional imagery (thesis 5).  

IMAGERY AND ITS IMPLEMENTATION  

This special technical use of imagery (not to be confused with the psychological term meaning the formation and manipulation mental images) refers to "our amazing mental ability to "structure" or "construe", a perceived situation in many alternate ways" [Langacker1988b], as opposed to traditional semantic approaches whose concern is with informational content alone. Thus "every conception reflects some particular construal of its content". Langacker identifies six important dimensions of imagery; in our semantic analysis of spatial expressions we are interested in just three of these:  

1. level of specificity  

2. scale and scope of predication  

3. perspective  

The remainder of this section is a characterization of each of these dimensions and the consequences that their consideration has with respect to the design of a conceptual representation for spatial expressions.  

REPRESENTING 3-D SPACE  

The basic cognitive domain relative to which the spatial meaning of projective prepositions is characterized, is structured three-dimensional space. In our system space is represented using an orthogonal axis system we refer to as the DCS (Domain Coordinate System). In the process of image construction conceptual objects will be constrained to locations described relative to the DCS. The DCS mirrors the speaker's perceptual assignment of axes to a scene, the x-axis extends from deictic left to deictic right, the y-axis from deictic front to deictic back, and the z-axis extends vertically.  

LEVEL OF SPECIFICITY  

The level of specificity of conventional imagery addresses the issue of the degree of detail with which an entity is characterized. Specificity has already been mentioned in connection with the construction of the network of polysemous senses of a lexical item; on the other hand, concerning different lexical items, we can readily identify different spatial predications that are schematic with respect to each other. Consider the sentences below.  

(a) The chair is near the desk.  

(b) The chair is in front of the desk.  

(c) The chair is facing the desk.  

Sentence (a) simply predicates proximity; (b) predicates both proximity and a positioning of the LO relative to a particular side of the RO; lastly (c) predicates proximity and a relative positioning of the LO with respect to the RO, with the additional anti-alignment of the front face normals of the two objects.  

Schematic contrast dictates the minimum degree of detail we must maintain in our computational representation of the conceptual reference and located objects. In sentences (a) the objects can be thought of as structureless points; in (b) the representation of the RO must incorporate the notion of sideness; and in (c) both the RO and LO are sided. We borrow Lang's conceptual representation of objects  

\footnote{The issue of which side of the reference object the located object is positioned with respect to is addressed as a consequence of the perspective dimension of conventional imagery}
termed object schemata [Lang1993], constructed
within Bierwisch's and Lang's the two-level se-
mantics [Bierwisch and Lang1989]. The object
schema for a desk is:

\[
\begin{align*}
a & \text{ max } b \text{ vert } c \text{ across} \\
a_1 & \text{ i-left } b_1 \text{ i-bottom } c_1 \text{ i-front} \\
a_2 & \text{ i-right } b_2 \text{ i-top } c_2 \text{ i-back} \\
d & \text{ i-front } d & \text{ i-right } d & \text{ i-back} \\
d_1 & \text{ i-left } d_{1} \text{ i-bottom } d_{1} \text{ i-top} \\
d_2 & \text{ i-right } d_{2} \text{ i-top } d_{2} \text{ i-bottom} \\
\end{align*}
\]

In this first schema a, b and c label three or-
thogonal axes centered at the object, each of which
can be instantiated by one or more dimensional as-
signment parameters (DAPs)\(^2\); a\(_1\)-a\(_2\), b\(_1\)-b\(_2\) and
c\(_1\)-c\(_2\) are corresponding half-axes. Each half axis
is labelled either nil or with an intrinsic side
(eg. i-front). This representation is augmented
with both a three-dimensional Cartesian coordi-
nate which when assigned locates the conceptual
schema relative to the DCS; and the values of the
default extents for the object type along the axes
a, b and c.

Imagery implies an imager, that is, the image
exists in and with respect cognitive world of
the speaker (by default) and this necessarily has
important consequences. With respect to spatial
language, issues pertaining to perspective, that is
taking account of the imager, include the speaker's
vantage point and orientation.

**ORIENTATION**

The interpretation of some spatial expressions is
dependent on assumptions as to the speaker's
orientation with respect to the objects in the
scene (eg. whether A is "to the left of" B in
a scene, is dependent on the orientation of the
speaker/viewer); other expressions are orientation
independent such as "above" and "below" which
implicitly refer to the downward pull of gravity
(al-
though in space verticality is speaker dependent).

When an object schemata is characterized rel-
relative to the DCS it is both assigned a Cartesian
position (as we show later), and its half-axes are
assigned deictic sides according to their relative
orientation with the observer. For example if a
desk is positioned "against the left wall" as in fig-
figure 1 this would result an instantiated conceptual
schema for the "desk" of:

\[
\begin{align*}
a & \text{ max } b \text{ vert } c \text{ across} \\
a_1 & \text{ i-left } b_1 \text{ i-bottom } c_1 \text{ i-front} \\
ad & \text{ i-front } d & \text{ i-right } d & \text{ i-back} \\
a_2 & \text{ i-right } b_2 \text{ i-top } c_2 \text{ i-back} \\
d_{1} & \text{ i-left } d_{1} \text{ i-bottom } d_1 \text{ i-top} \\
d_{2} & \text{ i-right } d_{2} \text{ i-top } d_{2} \text{ i-bottom} \\
\end{align*}
\]

Here a\(_1\) is the intrinsic left side but the deictic
front of the desk.

**VANTAGE POINT**

The speaker's vantage point is another factor that
determines the interpretation of spatial expres-
sions in a scene. The notions of deictic and intrin-
ic interpretations of projective prepositions
 can be accounted for purely by recognizing that in
each the speaker adopts a different vantage point.
For deictic interpretations the vantage point is the
speaker's actual position. The vantage point for
intrinsic interpretations is the functionally rele-
vant position with respect to a reference object,
for example, "left of the desk" under the intrinsic
interpretation uses a vantage point that is directly
in front of the desk (the typical configuration when
a human uses a desk).

The meaning of a projective preposition is
conceptually represented as a spatial constraint on
the conceptual schema of the located object which
extends out from a particular side of a reference
object, the precise nature of which we describe in
the next subsection. In our system the lexicalized
constraint is of the form of a two place predicate:
\(< \text{ zoneprox } X : \text{ side } Y >\>

Where X is the reference object and Y the loc-
located object. The parameter side depends on
the preposition. Thus the schematicity we observed in
section is explicitly represented:

\[\begin{align*}
(a) & \text{ Y is near X.} \\
& < \text{ zoneprox } X : \text{ Y } > \\
(b) & \text{ Y is in front of X.} \\
& < \text{ zoneprox } X : \text{ front } Y > \\
(c) & \text{ Y is facing X.} \\
& < \text{ zoneprox } X : \text{ front } Y : \text{ back } > \\
\end{align*}\]

**SCOPE OF PREDICATION**

Scope refers to exactly how much of a cognitive
domain is included in the characterization. Mini-
ally, the scope of an image for "next to" must en-
compass at least the reference and subject objects
and some region of space separating them. We im-
plement the spirit of this concept by realising the
lexicalized constraint for a projective preposition
as a potential field fixed at the reference object's
position in the DCS\(^3\). The proximity and direc-
tional nature of the constraint \(< \text{ zoneprox } .. >\>
 is captured using a potential field \(P_x\), where:

\[d_e = (x - x_0)\]  \hspace{1cm} (1)

\(^3\)This technique is borrowed from robot manipu-
lator path-planning [Khatib1986]
Here the \( x \)-axis points direction of the half-
axis of the particular side of the reference axis in
the DCS; and in the case of "in front of" \( y \) is the
perpendicular direction in the horizontal plane;
\((x_0, y_0)\) is the Cartesian coordinate of the refer-
ence object in the DCS, and lower the value of \( P_x \)
for a location \((x, y)\) for the located object the
better the spatial constraint is satisfied. The mini-
num for the field can be quickly computed using
gradual approximation [Yamada et al. 1988]. The
values of \( K_{\text{proz} x} \), \( L_{\text{proz} x} \), and \( K_{\text{dir} x} \) are depen-
dent on the located and reference objects and are
set on the basis of scale considerations (see ). Mul-
tiple spatial predications over an object is simply
accommodated within the potential field model by
linear addition of component fields.

**SCALE OF PREDICATION**

The concept of the scale relates to the object de-
pendency of the degree of proximity and direc-
tional constraint afforded by a preposition: where
"X is left of Y", and X and Y are houses, then this
meaning of this predication would contrast with its
meaning if X and Y were pieces of fruit. The con-
cept of proximity and directional constraint predi-
cated by "left of" is apparent in both cases, what
differs is the scale relative to which it is character-
ized.

Scale effects are realised in the mechanism by
which the constants of the potential field are set.
For the potential field \( P_x \), the effect of the con-
stants on the nature of the constraint are:

1. \( K_{\text{proz} x} \)
   Proportional to range of the possible separa-
tions of X and Y that would still satisfy the pre-
dication.

2. \( L_{\text{proz} x} \)
   The default separation of X and Y.

3. \( K_{\text{dir} x} \)
   Proportional to the range of directions that
   would still satisfy the predication.

Thus for a reference object that is a house
\( K_{\text{proz} x} \), \( L_{\text{proz} x} \), \( K_{\text{dir} x} \) must all be consider-
ably greater than for a piece of fruit. The precise
values can only reasonably set as a result of some
experimental investigation, currently \( K_{\text{proz} x} \) and
\( L_{\text{proz} x} \) are linearly dependent on the sum of the
extents of the reference and subject objects in the
direction of spatial alignment; and \( K_{\text{dir} x} \) on the
perpendicular extent of the reference object in the
plane of the constraint.

**GENERATING DEPICTIONS**

After using gradual approximation to find the po-

tion of the minimum in the potential fields rep-

tresenting the spatial predications over a particular
object, this point can be regarded as a probable
interpretation. By tying each conceptual object
to a graphical model, and interpreting the DCS
as the viewer's perceptual axis system, conceptual
interpretations can be rendered as scene de-

pictions. Figure 2 illustrates one depiction of the
cumulative interpretation of the following verbal
description, in which all projective prepositions
are viewed intrinsically.

"I am in a room. Against the left wall is a
long desk. Against the back wall is a short desk.
In front of the long desk is a chair. Another chair
is to the left of the long desk. The chair in front
of the desk is near the short desk."

**OTHER APPROACHES AND CLOSING REMARKS**

Nearly all the work in recent years on computing
the meanings of spatial prepositions stem from the
prototype

semantics of either Herskovits [Herskovits1985],
[Herskovits1986] or Talmy [Talmy1983]. Schirra
[Schirra and Stopp1993] adopts Herskovits' notion
of a core meaning, and implements this as a typ-
icality field. The ability to sum fields of different
predications satisfies the compositionality require-
ment. Yet representational poverty exists with re-

spect to the spatial and perceptual characteristics
of the objects, as while directionality and prox-
imity constraints are adequately captured for
the intrinsic reference frame and set of objects, varia-
tion in the degree of constraint (for example, de-

pending on the size of the reference object) and
the potential for ambiguity arising from interpre-
tations with respect to different reference frames
are not accounted for.

Underling Kalita's work [Kalita and Badler1991] is a conceptualiza-

tion of the space around a reference object as six

4Natural language sentences are parsed to three
branch quantifiers using a prolog DCG grammar, the
logical predicates are the input to the cognitive seman-
tic processor, the resulting conceptual representations
are converted to depictions in by the depiction module
. The cognitive semantic processor and the depiction
module are implemented in Smalltalk/Objectworks
orthogonal rectangular projected regions (based upon an enclosing cuboid idealization of the object) due to Douglas [Douglas and Novick1987]. Using this model and following Talmy's work, the semantics of projective prepositions are lexicalized as geometric-relation schemas. Reference frame ambiguity is not addressed; directionality is too tightly restricted to one of the six rectangular regions, and proximity constraint is left to the "underlying constraint satisfaction techniques and the use of a weight slot in the template for constraint representation".

Within the framework of the LILOG project [Maienborn1991] Ewald Lang implemented the two-level approach to the semantics of dimensional adjectives in which the perceptual and dimensional properties of objects are conceptually represented as object schemata [Bierwisch and Lang1989]. Further developed for projective spatial predications, Lang's object schemata are capable of distinguishing deictic and intrinsic readings, though without explicit reference to a quantitative space (i.e. actual scenes and observers) as in the case of Schirra and Kalita.

Our system represents a first attempt, and very highly specialized implementation, of the conventional imagery process that is a component of the cognitive grammarian's view of linguistic semantics. Its performance, in terms of generating all possible interpretations, and the quality of the interpretations constitutes a significant advance on previous approaches.

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