Scalar Dark Matter, GUT baryogenesis and Radiative neutrino mass

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Abstract

We investigate an interesting correlation among dark matter phenomenology, neutrino mass generation and GUT baryogenesis, based on the scotogenic model. The model contains additional right-handed neutrinos $N$ and a second Higgs doublet $\Phi$, both of which are odd under an imposed $Z_2$ symmetry. The neutral component of $\Phi$, i.e. the lightest of the $Z_2$-odd particles, is the dark matter candidate. Due to a Yukawa coupling involving $\Phi$, $N$ and the Standard Model leptons, the lepton asymmetry is converted into the dark matter asymmetry so that a non-vanishing $B - L$ asymmetry can arise from ($B - L$)-conserving GUT baryogenesis, leading to a nonzero baryon asymmetry after the sphalerons decouple. On the other hand, $\Phi$ can also generate neutrino masses radiatively. In other words, the existence of $\Phi$ as the dark matter candidate resuscitates GUT baryogenesis and realizes neutrino masses.

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I. INTRODUCTION

The origin of the observed baryon asymmetry can not be accounted for within the Standard Model (SM) and is one of the unresolved issues in particle physics and cosmology. The simplest Grand Unified Theory (GUT) based on the SU(5) model, proposed by Georgi and Glashow in 1974 [1], features leptoquark gauge bosons which do mediate baryon number violating processes, leading to proton decay. The model, however, conserves the difference between the baryon and lepton number $B - L$. In other words, any generation of a baryon asymmetry from heavy gauge or Higgs boson decays, as discussed in Refs. [2–5], comes with an equal amount of lepton asymmetry. These baryon and lepton asymmetries, however, will be washed out completely by non-perturbative sphaleron processes [6–8], which come into thermal equilibrium when the temperature of the universe drops roughly below $10^{12}$ GeV. The $B - L$ symmetry conservation also exists in larger symmetry groups, such as $SO(10)$, where the abelian $U(1)_{B-L}$ is a subgroup. Therefore, as long as $U(1)_{B-L}$ is not broken when a baryon asymmetry is created, i.e., initially $B + L \neq 0$ but $B - L = 0$, such a baryon asymmetry will not survive the sphaleron processes.

In principle, there are at least two ways to revive GUT baryogenesis. First, nonzero $B - L$ can still be realized in certain matter representations under $SO(10)$ or larger groups as demonstrated, for instance, in Refs [9–14]. Second, Fukugita and Yanagida [15] (and a recent update, Ref. [16]) have proposed to include right-handed neutrinos to resuscitate GUT baryogenesis, where the right-handed neutrino $N$ can be embedded into $SU(5)$ as a singlet or into the $16$ of $SO(10)$. A Majorana mass of $N$, which can arise from the spontaneous symmetry breaking of $L$ via the vacuum expectation value of a scalar or can simply be imposed by hand, explicitly violates the original $B - L$ symmetry.

In this paper, we revisit and extend the idea of Fukugita and Yanagida [15] in the context of the scotogenic model [17]. In this model, a second scalar $SU(2)_{L}$ doublet $\Phi$ is introduced which radiatively generates neutrino masses as shown in Fig. 1. At the same time, the neutral component of the doublet is a suitable dark matter (DM) candidate because of an imposed $Z_2$ symmetry.

In that both $\Phi$ and right-handed neutrinos $N$ are $Z_2$-odd, the type-I seesaw Yukawa cou-
FIG. 2: $N$-mediated lepton number violating processes which transfer a $L$ asymmetry into that of DM ($\Phi$).

The $y\ell HN$ coupling is forbidden ($\ell$: SM lepton doublet) but a new Yukawa coupling $y\ell\Phi N$ is allowed, which induces a washout of lepton number. As illustrated in Fig. 2, the change of the lepton number is accompanied by a change of the $\Phi$ number, $\Delta L = \Delta \Phi$. In other words, the $L$ asymmetry is transferred into a DM asymmetry. Moreover, part of the DM asymmetry further shifts to an asymmetry of the Higgs boson because of the $\Phi - H$ interactions: $\Phi^* H \leftrightarrow \Phi H^*$ and $\Phi^{(*)}\Phi^{(*)} \leftrightarrow H^{(*)}H^{(*)}$. In this scenario, the $L$ asymmetry can be maximally reduced down to one third of the initial value (instead of one-half in the case without $\Phi$) since $\Phi$ and $H$ share the asymmetry. That is, the resulting final $B - L$ asymmetry can be maximally one third of the initial $B + L$ asymmetry generated by GUT baryogenesis. Taking into account the top (bottom) Yukawa coupling, which is in thermal equilibrium for temperatures $T \lesssim 10^{16}$ ($10^{12}$) GeV, the $H$ asymmetry will be transferred into quarks, leading to a larger lepton number washout. See Ref. [15] for more details.

FIG. 3: Pictorial illustration of asymmetry conversion in the presence of DM $\Phi$ and the right-handed neutrino $N$. The $L$ asymmetry generated from GUT baryogenesis is converted into a DM ($\Phi$) asymmetry, and then is also shared by $H$ due to $\Phi - H$ equilibrium. As a result, the maximal $B - L$ asymmetry is one third of the initial $B + L$ asymmetry from GUT baryogenesis as indicated in the middle panel. If DM decouples before the EWPT, the asymmetry will be transferred back to the SM sector, increasing the final $B$ asymmetry as displayed in the right panel, where the solid (dashed) line corresponds to DM freeze-out before (after) the EWPT. See the text for more details.

If DM decouples from the thermal bath before the electroweak phase transition (EWPT), the DM asymmetry will be transformed back to $H$ via the process $\Phi H^* \leftrightarrow \Phi^* H$, which has
only a single power of Boltzmann suppression and is very efficient compared to the doubly Boltzmann-suppressed annihilation channels $\Phi\Phi^* \leftrightarrow HH^*$ and $\Phi^{(*)}\Phi^{(*)} \leftrightarrow H^{(*)}H^{(*)}$. This conversion will slightly increase the final baryon asymmetry because the Yukawa couplings and the sphalerons will redistribute the asymmetries among quarks, leptons and Higgs bosons. Note that after the EWPT, the asymmetry for the real part of the neutral component $H^0$ will vanish because of the Higgs vacuum expectation value \[18\], whereas the remaining degrees of freedom of $H$ will become the longitudinal component of $W^\pm$ and $Z$. Similarly, the $\Phi^0$ (neutral components of $\Phi$) asymmetry will also vanish after the EWPT due to the efficient $\Phi - H$ interactions\(^\text{1}\) while the $\Phi^\pm$ (charged components) asymmetry will move to $W^\pm$. The final $B$ and $L$ asymmetries will stay unchanged since the sphalerons become ineffective after the EWPT. Fig. 3 elucidates the asymmetry transformation as a function of time. On the other hand, the DM relic abundance is mainly determined by the Higgs-DM couplings for TeV DM (such that DM freezes out prior to the EWPT) as shown in Fig. 4.

\[\begin{align*}
\Phi^* & \leftrightarrow \Phi & \leftrightarrow H & \Phi^{(*)} & \leftrightarrow H^{(*)} \\
\Phi & \leftrightarrow \Phi^* & \leftrightarrow H^* & \Phi^{(*)} & \leftrightarrow H^{(*)} \\
\end{align*}\]

FIG. 4: Main DM annihilation processes which determine the DM density. The $\lambda$’s denote the Higgs-DM quartic couplings, defined in Eq. (II.2).

This paper is organized as follows. In Section II, we briefly review the scotogenic model and then develop the formalism for lepton number washout based on Boltzmann equations in Section III. In Section IV, we explain how asymmetries are transferred between the DM and SM sectors and present our numerical results of the Boltzmann equations. The relic abundance is calculated in Section V where the DM direct search bounds from the XENON1T experiment are also taken into account. Finally, we conclude in Section VI.

II. SCOTOGENIC MODEL

The scotogenic model has been proposed by E. Ma \[17\], where the neutrino mass is loop-induced by a second $SU(2)_L$ doublet scalar $\Phi$ and the right-handed neutrinos $N$, both of which are odd under an imposed $Z_2$ symmetry. Thus, Yukawa couplings in the type-I seesaw, $y_{ij}\ell_iH^*N_j$ are forbidden and replaced by $y'_{ij}\ell_i\Phi^*N_j$. In principle both the $Z_2$-odd $N$ and the neutral component of the $\Phi$ doublet could be the DM candidates. However, the mass of $N$ being of interest for this work is above $10^{10}$ GeV, that is too heavy to thermally generate

\[^{1}\text{The interaction } \Phi^0h \leftrightarrow \Phi^{(*)}h (h: \text{SM Higgs boson after the EWPT) will erase the asymmetry stored in } \Phi^{(*)}.\]
the correct relic density \[19\]. In the framework of \( SU(5) \), \( \Phi \) can be embedded into the representation of 5, while \( N \) can be a singlet. We here simply assume that other particles, which are embedded in the same representation of \( SU(5) \) (or larger symmetry groups) as SM particles or \( \Phi \), are heavier than the scale of interest. Thus, only the SM particles, \( \Phi \) and \( N \) are taken into account in the analysis.

In addition to the SM interactions, the Lagrangian reads

\[
\mathcal{L} \supset y'_{ij} \bar{\ell}_i \Phi^* N_j + \frac{M_{N_k}}{2} \overline{N_k}^c N_k + V(\Phi, H),
\]

with

\[
V(H, \Phi) = \mu_1^2 |H|^2 + \mu_2^2 |\Phi|^2 + \lambda_1 |H|^4 + \lambda_2 |\Phi|^4 + \lambda_3 |H|^2 |\Phi|^2 + \lambda_4 |H^* \Phi|^2 + \frac{\lambda_5}{2} (\langle H^* \Phi \rangle^2 + \text{h.c.}),
\]

which is just the scalar potential of the inert Higgs Doublet model \[20\]. The radiative neutrino mass matrix induced by loops of \( \Phi \) and \( N \) is \[17\]

\[
(m_\nu)_{ij} = \sum_k \left( y'_{ik} y'_{jk} \right)^* \frac{M_{N_k}}{16 \pi^2} \left( \frac{m_R^2}{m_R - M_{N_k}^2} \log \frac{m_R^2}{M_{N_k}^2} - \frac{m_I^2}{m_I - M_{N_k}^2} \log \frac{m_I^2}{M_{N_k}^2} \right),
\]

where

\[
m_R^2 = \mu_2^2 + \frac{1}{2} (\lambda_3 + \lambda_4 + \lambda_5) v^2,
\]

\[
m_I^2 = \mu_2^2 + \frac{1}{2} (\lambda_3 + \lambda_4 - \lambda_5) v^2,
\]

with \( v = 246 \) GeV being the Higgs vacuum expectation value. Note that in order to obtain a non-vanishing neutrino mass, one must have \( m_R \neq m_I \), i.e., \( \lambda_5 \neq 0 \). We here are interested in the region of \( M_N \gtrsim 10^{10} \) GeV, \( m_R \sim m_I \sim \text{TeV} \) and \( |m_R - m_I| \ll m_I \sim m_R \). In this case, the neutrino mass matrix becomes

\[
(m_\nu)_{ij} = \frac{\lambda_5 v^2}{16 \pi^2} \sum_k \left( y'_{ik} y'_{jk} \right)^* \left( \log \left( \frac{M_{N_k}^2}{m_0^2} \right) - 1 \right),
\]

where \( m_0 = \frac{m_R + m_I}{2} \). To reproduce the observed neutrino mass squared difference responsible for atmospheric neutrino oscillations, the heaviest neutrino must be heavier than 0.05 eV or so, which corresponds to \( \lambda_5 \sim 3 \times 10^{-3} \) for \( M \sim 10^{12} \) GeV and \( m_0 \sim \text{TeV} \), given \( y' \) of \( \mathcal{O}(1) \).

### III. Washout Formalism

Due to the Hubble expansion, a convenient quantity to describe the particle number density is \( Y \equiv n/s \), which is the number density normalized to the entropy density \( s \), i.e., the number
per co-moving volume. The density \( Y \) is conserved in the absence of particle creation or annihilation. The Boltzmann equation of a particle \( \ell \) for an interaction \( \ell a_1 \cdots a_n \leftrightarrow f_1 \cdots f_m \) is,

\[
 z H s \frac{dY_\ell}{dz} = - \sum_{a_i, f_j} [\ell a_1 \cdots a_n \leftrightarrow f_1 \cdots f_m], \tag{III.1}
\]

where \( H \) is the Hubble parameter, \( z = M_N / T \), and

\[
 [\ell a_1 \cdots a_n \leftrightarrow f_1 \cdots f_m] = \frac{n_{\ell} n_{a_1} \cdots n_{a_n}}{n_{\ell} n_{a_1} \cdots n_{a_n}} \gamma^{eq}(\ell a_1 \cdots a_n \leftrightarrow f_1 \cdots f_m)
\]

\[
 \quad - \frac{n_{f_1} \cdots n_{f_m}}{n_{f_1} \cdots n_{f_m}} \gamma^{eq}(f_1 \cdots f_m \leftrightarrow \ell a_1 \cdots a_n). \tag{III.2}
\]

The thermal rate \( \gamma^{eq} \) is defined as

\[
 \gamma^{eq}(\ell a_1 \cdots a_n \rightarrow f_1 \cdots f_m) = \left[ \int \frac{d^3 p_\ell}{2E_\ell(2\pi)^3} e^{-E_\ell/T} \right] \prod_{a_i} \left[ \int \frac{d^3 p_{a_i}}{2E_{a_i}(2\pi)^3} e^{-E_{a_i}/T} \right] \times \prod_{f_j} \left[ \int \frac{d^3 p_{f_j}}{2E_{f_j}(2\pi)^3} \right] \times (2\pi)^4 \delta^4(p_\ell + \sum_{i=1}^n p_{a_i} - \sum_{j=1}^m p_{f_j}) |M|^2; \tag{III.3}
\]

where \( |M|^2 \) is the squared amplitude summing over initial and final spins.

To simplify the analysis, we consider a 1+1 scenario, i.e., one generation of the SM leptons and one right-handed neutrino\(^2\). Moreover, we assume that the scale of GUT baryogenesis is slightly below the right-handed neutrino mass to avoid complications from finite-temperature effects (if, for example, the decay \( N \rightarrow HL \) would be kinematically forbidden, the first processes in Fig. 2 would not have resonance anymore, reducing the \( L \) washout effect) due to thermal masses when \( T \gtrsim m_N \) \([21]\).

For the \( L \) washout computation, we include both \( \Delta L = 1 \) and \( \Delta L = 2 \) interactions. Following the notation of Ref. \([21]\), the \( \Delta L = 2 \) washout processes include \( \ell \Phi \leftrightarrow \ell \Phi^* \) (with thermal rate \( \gamma_{NS} \)) and \( \ell \ell \leftrightarrow \Phi^* \Phi^* \) (\( \gamma_{NI} \)) as displayed in Fig. 2. The relevant \( \Delta L = 1 \) washout processes are \( \ell \Phi \leftrightarrow N \) (\( \gamma_D \)), \( \ell N \leftrightarrow \Phi^* A \) (\( \gamma_{AA} \)), \( \ell \Phi \leftrightarrow NA \) (\( \gamma_{A1} \)) and \( \ell A \leftrightarrow N \Phi^* \) (\( \gamma_{A2} \)). We refer readers to our previous work \([16]\) and references therein for more details. Note that the previous work is based on the type-I seesaw mechanism while in this work, it is another Yukawa coupling \( y' \ell \Phi^* N \) that is responsible for the washout processes. The formalism of washout computation is, however, similar for the two cases.

The resulting Boltzmann equations including the lepton washout and sphalerons \([22, 23]\) processes read

\(^2\) For simplicity, we stick to the cases where the initial lepton asymmetry is stored in the lepton doublet.
\[ z H s \, \frac{dY_{B-L}}{dz} = 2 \left( 2 \gamma_{N s} + 4 \gamma_{N t} + \frac{\gamma_A s + \gamma_A t_1 + \gamma_A t_2}{Y_{N s}^{eq}} \right) \frac{Y_{B+L} - Y_{B-L}}{2 Y_{L}^{eq}} \]

\[ - 2 b \Phi \left[ \gamma_{N s} + 4 \gamma_{N t} + \gamma_A s + \gamma_A t_1 + \gamma_A t_2 \right] \frac{Y_{N s}^{eq}}{Y_{\Phi}^{eq}}, \quad (III.4) \]

\[ z H s \, \frac{dY_{B+L}}{dz} = - 2 \left( 2 \gamma_{N s} + 4 \gamma_{N t} + \frac{\gamma_A s + \gamma_A t_1 + \gamma_A t_2}{Y_{N s}^{eq}} \right) \frac{Y_{B+L} - Y_{B-L}}{2 Y_{L}^{eq}} \]

\[ + 2 b \Phi \left[ 2 \gamma_{N s} + 4 \gamma_{N t} + \gamma_A s + \gamma_A t_1 + \gamma_A t_2 \right] \frac{Y_{N s}^{eq}}{Y_{\Phi}^{eq}} \frac{351}{2} \alpha_{W}^{5} \frac{m_{N s}}{z} Y_{B+L} \cdot (III.5) \]

\[ z H s \, \frac{dY_{N}}{dz} = - \left( \gamma_D + 4 \gamma_{A s} + 4 \gamma_A t_1 + 4 \gamma_A t_2 \right) \left( \frac{Y_{N}}{Y_{N s}^{eq}} - 1 \right) \cdot (III.6) \]

\[ \frac{dY_{\Phi}'}{dz} \equiv \frac{dY_{B-L}}{dz} \cdot (III.7) \]

where \( Y_{L(B)} \equiv Y_{\text{lepton (baryon)}} - Y_{\text{anti-lepton (anti-baryon)}} \) and \( Y_{\text{eq}} \) is the equilibrium density of the corresponding (anti-)particle. The impact of the \( t \)- and \( b \)-Yukawa couplings on the washout processes can be characterized by the factor \( b \Phi \) \[^{16} \]

\[ b \Phi = \begin{cases} \frac{1}{3} & 10^{12} \lesssim T \lesssim 10^{16} \text{ GeV} \\ \frac{1}{5} & T \lesssim 10^{12} \text{ GeV} \end{cases} \cdot (III.8) \]

Moreover, the chemical equilibrium for \( \Phi^{(*)} \Phi^{(*)} \leftrightarrow H^{(*)} H^{(*)} \) is reached if

\[ \frac{\lambda_{5}^{2} T}{8 \pi} \gtrsim \frac{T^{2}}{m_{W}^{2}}, \quad (III.9) \]

with \( m_{W} = 1.22 \times 10^{19} \text{ GeV} \). The \( \Phi - H \) chemical equilibrium is always fulfilled for values of \( \lambda_{5} \) of interest.

The final \( B \) and \( L \) asymmetries as functions of the final \( B - L \) asymmetry are

\[ Y_{B}^{\text{final}} = c_s Y_{B-L}^{\text{final}}, \quad Y_{L}^{\text{final}} = (c_s - 1) Y_{B-L}^{\text{final}}. \cdot (III.10) \]

For non-supersymmetric models the sphaleron conversion factor is \( c_s = 28/79 \) \[^{18,24} \] if DM decouples before the EWPT. On the other hand, if DM freezes out after the EWPT, the \( \Phi^{0} \) (\( \Phi^{\pm} \)) asymmetry will just vanish (transfer into \( W^{\pm} \)), and has no influence on the final \( B \) and \( L \) asymmetries as explained above. In this case, one has \( c_s = 8/23 \) as we shall see below.

**IV. ASYMMETRY TRANSFER BETWEEN DM AND SM SECTORS**

We now are in the position to explain how the washout processes can create a nonzero \( B - L \) asymmetry and how asymmetries are transferred among different particles.

For temperatures above \( 10^{12} \text{ GeV} \), the \( (B + L) \)-violating\(^3\) sphalerons are not in thermal equilibrium and part of the lepton asymmetry is moved to DM due to the washout processes

\(^3\) In the following, we will use the shorthand notations \( B+L, B \) and \( L \) for \( (B + L)-, B- \) and \( L\)-violating, respectively.
induced by the Yukawa coupling $y'\bar{\ell}\Phi N$. For both of the $\Delta L = 1$ and $\Delta L = 2$ interactions, the change in the lepton number comes with an equal amount of the DM number change. The partial asymmetry of $\Phi$ is further converted into $H$ through the interaction, $\frac{\lambda_5}{2} ((H^\ast \Phi)^2 + \text{h.c.})$. That is, after $L$ washout one obtains a nonzero $B - L$ asymmetry: $\Delta (B - L) = -(\Delta \Phi + \Delta H)$.

For the washout calculation, $\lambda_5 = 1$ is assumed such that the $\Phi - H$ interactions are always in chemical equilibrium during the period of washout, i.e., $\Delta (B - L) = -2\Delta \Phi$. The numerical results are presented in Fig. 6 with the initial $B + L$ asymmetry from GUT baryogenesis injected at the scale of $M_N/3$ (left panel) and $M_N/10$ (right panel). The contours represent the ratio of the final $B - L$ to the initial $B + L$ asymmetry, i.e., $Y^\text{final}_{B-L}/Y^\text{initial}_{B+L}$. A smaller $B + L$ injection scale implies a shorter $L$ washout period before the sphalerons kick in, and hence requires a larger Yukawa coupling (a higher washout rate) to compensate. As a result, the $Y^\text{final}_{B-L}/Y^\text{initial}_{B+L}$ contours move upward in the right panel when compared to the left one.

Maximal $L$ washout (the maximal final $B - L$ asymmetry) denoted by dark red areas arises from the case in which the $L$ processes are very efficient before the sphalerons come into play but become ineffective when the sphalerons are in thermal equilibrium. Two minimal $B - L$ asymmetry scenarios (white areas) correspond to situations where first $L$ washouts have never been fast enough before the sphalerons destroy most of the initial $B + L$ asymmetry, and second both $L$ and $B + L$ processes are present and effective for a long time, leading to vanishing $B$ and $L$ asymmetries\(^4\). The black solid line indicates the active neutrino mass $m_\nu$ of 0.23 eV, the bound from Planck \(^{25}\) on the sum of the active neutrino masses, while the black dashed line corresponds to $m_\nu = \sqrt{\Delta m^2_{\text{atm}}} \simeq 0.05$ eV and the black dotted line for $m_\nu = \sqrt{\Delta m^2_{\text{sol}}} \simeq 8.6 \times 10^{-3}$ eV. If $\lambda_5$ is increased (decreased), according to Eq. (II.6) the black lines will move downwards (upwards) accordingly.

In order to obtain $m_\nu = 0.05$ eV and $Y^\text{final}_{B-L}/Y^\text{initial}_{B+L} \gtrsim 10^{-2}$, $M_N$ has to be roughly above $10^{13}$ GeV with $y' \sim 0.1$. In our previous work \(^{16}\) with the type-I seesaw Yukawa coupling $\bar{\ell}H^\ast N$, one can achieve larger washout effects with $Y^\text{final}_{B-L}/Y^\text{initial}_{B+L} \gtrsim 10^{-1}$ and at the same time reproduce $m_\nu = 0.05$. The main difference in the presence of $\Phi$ is that the active neutrino mass is loop-induced and hence a larger Yukawa coupling is needed. In this case, the washout processes last for a longer time and coexist with the $B + L$ sphalerons, leading to a smaller $B - L$ asymmetry.

Depending on the initial $B + L$ asymmetry, there exist regions of the parameter space capable of reproducing $Y^\text{final}_{B-L} \simeq 2.4 \times 10^{-10}$ to account for the observed baryon asymmetry, $Y^\text{final}_B = 8.7 \times 10^{-11}$ \(^{25}\). Assuming that, for example, the initial $B + L$ asymmetry is of order $10^{-6}$ and the $B + L$ injection scale is $M_N/10$, $M_N$ can be as low as $10^{10}$ GeV to realize both the baryon asymmetry and the neutrino mass. In this case $L$ washouts can still be efficient enough to generate a non-vanishing $B - L$ asymmetry before the sphalerons destroy the entire $B + L$ asymmetry.

When the temperature drops below $10^{12}$ GeV and becomes much smaller than $M_N$, $L$ washouts are ineffective but the sphaleron processes start to destroy the $B + L$ asymmetry.

\(^4\) Again, the detailed analysis can be found in our previous work, Ref. \(^{16}\), with the different particle contents but with a similar washout mechanism.
Later on, SM Yukawa couplings reach equilibrium to rearrange the asymmetry among leptons, quarks and the Higgs boson. One can repeat the analysis of chemical equilibrium done in Refs. [18, 24, 26], including an extra constraint, $\mu_\Phi = \mu_H$. To simplify the analysis, we assume universal chemical potentials $\mu_\ell$ and $\mu_{eR}$ for the three left-handed lepton doublets and three right-handed leptons, respectively, and all the Yukawa couplings are in thermal equilibrium. This yields

$$\begin{align*}
\mu_q &= -\frac{1}{3}\mu_\ell, \\
\mu_{uR} &= \frac{1}{6}\mu_\ell, \\
\mu_{dR} &= -\frac{5}{6}\mu_\ell,

\mu_{eR} &= \frac{1}{2}\mu_\ell, \\
\mu_H &= \frac{1}{2}\mu_\ell, \\
\mu_\Phi &= \frac{1}{2}\mu_\ell,
\end{align*}$$

(IV.1) 

and thus the final $B$ and $L$ asymmetries are

$$\begin{align*}
B_f &= \frac{8}{23} (B - L), \\
L_f &= -\frac{15}{23} (B - L),
\end{align*}$$

(IV.3)

which is different from the case in the absence of $\Phi$ with $B_f = \frac{28}{79} (B - L)$ and $L_f = -\frac{51}{79} (B - L)$ [18, 24, 26] for the SM. That is to say, $\Phi$ shares the asymmetry and slightly reduces the baryon asymmetry for a given $B - L$ asymmetry.

Finally, when the temperature falls below $m_\Phi$, $\Phi$ begins to freeze out of the thermal bath. The DM relic density will be mainly determined by the quartic couplings $\lambda_{3,4,5}$ in Eq. (II.2), if they are large compared to the gauge couplings and Yukawa couplings. In other words, the
DM particle dominantly annihilates into the Higgs bosons. The interaction terms of \( \lambda_3 \) and \( \lambda_4 \) apparently will not change any asymmetries in \( \Phi \) and \( H \) while the \( \lambda_5 \) term, corresponding to \( \Phi H^* \leftrightarrow \Phi^* H \) and \( \Phi^+(s) \Phi^+(s) \leftrightarrow H^+(s) H^{+(s)} \), will shift the asymmetry from \( \Phi \) to \( H \). Note that the interaction \( \Phi H^* \leftrightarrow \Phi^* H \) is always much faster than the DM annihilation processes if \( \lambda_{3,4,5} \) are of the same order. That is because the former interaction is singly Boltzmann-suppressed but the latter ones are doubly suppressed. The asymmetry conversion between \( \Phi \) and \( H \) during freeze-out can be understood in the following simple ways. Since \( \Phi \) and \( H \) carry the same \( U(1)_Y \) charge, the disappearance of \( \Delta \Phi \) has to be compensated by the equal amount of \( \Delta H \) so that the total \( U(1)_Y \) is conserved.

In the case where DM freezes out before the EWPT, the \( \Phi \) asymmetry will be transformed into that of \( H \) and further into those of the quarks and leptons. On the other hand, if DM freeze-out takes place after the EWPT, due to the \( \Phi - H \) interactions the \( \Phi^0 \) asymmetry will simply vanish while the \( \Phi^\pm \) asymmetry will transfer to that of \( W^\pm \). Due to the fact that the sphaleron effects are not effective anymore below the EWPT, both the \( L \) and \( B \) asymmetries are conserved quantities independent of the \( \Phi \) asymmetry. The final baryon number will slightly increase by 2% if DM decouples before the EWPT and hence the asymmetry conversion occurs.

We would like to emphasize that regardless of the decoupling time of DM, the final DM abundance is not related to the baryon asymmetry, even if the initial DM asymmetry is closely connected to the initial \( B-L \) (also \( B \)) asymmetry. This is the price we have to pay in order to radiatively generate non-zero active neutrino masses via a non-zero \( \lambda_5 \). If \( \Phi \) decouples before the EWSB the interaction of \( \lambda_5 \) quickly shifts the \( \Phi \) asymmetry into that of \( H \) as the density of \( \Phi \) and \( \Phi^* \) decrease during freeze-out. Hence the final density of \( \Phi \) is only determined by the annihilation of \( \Phi \) and \( \Phi^* \), similar to symmetric DM scenarios. If \( \Phi \) decouples after the EWPT the asymmetry stored in \( \Phi^0 \) and \( \Phi^{0*} \) just vanishes due to the \( \Phi - H \) interactions as explained above. In addition, a non-zero \( \lambda_5 \) will result in a mass splitting between the two neutral components as indicated in Eq. (II.5). Thus the lightest neutral component is the DM particle, which is real and is its own antiparticle. The final DM density will only be determined by the DM annihilation into two Higgs bosons. Note that a zero \( \lambda_5 \) would yield correlation between the final DM abundance and the baryon asymmetry. In this case, the DM mass has to be around 5 GeV to reproduce the correct relic abundance. As \( \Phi \) is a \( SU(2) \) doublet, the \( Z \) boson can decay into \( \Phi \Phi^* \), increasing the \( Z \) decay width. This, however, will be excluded by the LEP bound. In other words, an asymmetric DM scenario cannot be realized in this framework.

V. DM RELIC DENSITY AND DIRECT DETECTION

In this section, we compute the DM relic density and discuss direct search bounds. The study of DM phenomenology for inert Higgs doublet models after electroweak symmetry breaking has been studied, for instance, in Refs. [27–30], while annihilation cross-sections in an unbroken phase have been computed in Ref. [31]. We here focus on the scenario in the latter case where TeV \( \Phi \) decouples before the EWPT and the main annihilation channels are
$\Phi \Phi^* \rightarrow HH^*$ and $\Phi^{(*)} \Phi^{(*)} \rightarrow H^{(*)} H^*$ as shown in Fig. 4. As we shall see later, to achieve the correct DM density, the DM-Higgs couplings $\lambda$'s have to be larger than unity and also than the gauge and Yukawa couplings. Thus, we neglect the gauge and fermion final states in the computation.

Since the $\Phi$ asymmetry is basically zero during (and after) freeze-out, the computation of the DM relic density $\Omega_\Phi + \Omega_{\Phi^*}$ is essentially the same as in the standard symmetric DM scenario and can be well approximated \[32, 33\] by

$$\Omega_{\text{DM}} h^2 \approx 2 \times 10^{-27} \, \text{cm}^3 \text{sec}^{-1} \left\langle \sigma v \right\rangle_{\Phi \Phi^* \rightarrow HH^*}.$$  

(V.1)

Here the thermally-averaged annihilation cross-section multiplied by the DM relative velocity is

$$\left\langle \sigma v \right\rangle_{\Phi \Phi^* \rightarrow HH^*} \approx \frac{\lambda_3^2}{32 \pi m_\Phi^2}.$$  

(V.2)

where we assume $\lambda_3 \gtrsim \lambda_5$ and $\lambda_4 = 0$ for simplicity. Note that the mass degeneracy among components of $\Phi$ will be lifted after electroweak symmetry breaking. Heavy components of $\Phi$ will decay into the lightest one but the total relic density stays constant due to the unbroken $Z_2$ symmetry.

![Image](image_url)

FIG. 6: Quartic coupling $\lambda_3$ versus DM mass $m_\Phi$. The blue line corresponds to the observed relic density while the red dashed area is excluded by the XENON1T direct search result \[34\]. The purple line represents the perturbativity limit $4\pi$.

On the other hand, $\Phi$ can interact with nucleons through the Higgs exchange and null results from DM direct searches put constraints on the DM-Higgs coupling $\lambda_3$. Again with the assumption of $\lambda_3 \gtrsim \lambda_5$ and $\lambda_4 = 0$, the DM-nucleon spin-independent cross-section is \[35\]

$$\sigma_{\text{SI}} = \frac{\lambda_3^2 f_N^2}{4 \pi} \frac{\mu^2 m_n^2}{m_h^4 m_\Phi^2},$$  

(V.3)
where $f_N = 0.3$, $\mu = m_n m_\Phi / (m_n + m_\Phi)$ and $m_n$ is the nucleon mass.

In Fig. we show the direct search bound from the XENON1T result \[34\] denoted by the red line and the blue line corresponds to the correct relic density, while the purple line is the perturbativity limit. It is clear that XENON1T is unable to probe the large DM mass region as the DM-nucleon cross-section is inversely proportional to the DM mass, leading to low sensitivity. In addition, the DM annihilation cross-section is also suppressed by the DM mass and $\lambda_3$ has to be large in order to reproduce the correct DM density. Thus, for a large DM mass $m_{DM} \gtrsim 19$ TeV the theory is not perturbative anymore. This roughly agrees with the result of Ref. \[31\], where 22.4 TeV is obtained by considering all contributions including the gauge bosons.

VI. CONCLUSIONS

In this work, we have explored an interesting correlation between DM, radiative neutrino masses and GUT baryogenesis, based on the scotogenic model \[17\]. The model contains a second Higgs doublet $\Phi$ together with right-handed neutrinos $N$, both of which are odd under a $Z_2$ symmetry. The lightest one of the $Z_2$-odd particles, $\Phi$, is a DM candidate. Due to the $Z_2$ symmetry, the type-I seesaw Yukawa coupling of the right-handed neutrinos to the Higgs boson is prohibited but a new coupling $y' \ell \Phi N$ ($\ell$ is the SM lepton doublet) is allowed. Consequently, the neutrino mass is radiatively induced by loops of $\Phi$ and $N$. In the context of $(B - L)$-preserving GUT baryogenesis, the additional interaction $\ell \Phi \leftrightarrow \bar{\ell} \Phi^*$ via $N$-exchange shifts the $L$ asymmetry into $\Phi$ such that a nonzero $B - L$ asymmetry can be generated. The net $B - L$ asymmetry will be preserved by the $(B + L)$-violating sphaleron effects and as a result the observed baryon asymmetry can be obtained.

Moreover, due to the interactions $\Phi^* H \leftrightarrow \Phi H^*$ and $\Phi^{(*)} \Phi^{(*)} \leftrightarrow H^{(*)} H^{(*)}$, the asymmetry in $\Phi$ from $L$ washouts will be further transferred into $H$ that helps to wash out more $L$, leading to a larger $B - L$ asymmetry. With two Higgs doublets, $\Phi$ and $H$, the induced $B - L$ asymmetry is at most one third (5/12 including the $t$- and $b$-Yukawa coupling effects) of the initial $B + L$ asymmetry from GUT baryogenesis, which is larger than the asymmetry obtained in Ref. \[15\], where the type-I seesaw Yukawa coupling is used to erase $L$ and to produce a nonzero $B - L$ asymmetry. Numerically, we have found that in order to generate a neutrino mass of $\sqrt{\Delta m_{atm}^2} \sim 0.05$ eV and achieve $Y_{B-L}^\text{final}/Y_{B-L}^\text{initial} \sim \mathcal{O}(10^{-2})$, the mass of the right-handed neutrino $M_N$ has to be roughly larger than $10^{13}$ GeV for TeV DM. If the initial $B + L$ asymmetry is sizable ($\gtrsim 10^{-6}$) and the $B + L$ injection scale is $M_N/10$, $M_N$ can be as low as $10^{10}$ GeV to accommodate both the baryon asymmetry and the neutrino mass, since $L$ washouts can still be efficient enough to create a non-vanishing $B - L$ asymmetry before the sphalerons completely destroy the $B + L$ asymmetry.

We have made sure that with TeV $\Phi$ masses one can reproduce the observed relic abundance which requires an $\mathcal{O}(1)$ coupling $\lambda_3$ and at the same time avoid the XENON1T direct search

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\[5\] The PandaX-II \[36\] and LUX \[37\] experiments yield similar limits, while the latest XENON1T result \[38\] only presents the bound for DM below 1 TeV.
bounds. In this case $\Phi$ falls out of equilibrium before the electroweak symmetry breaking and the asymmetry stored in $\Phi$ will convert back into $H$. That slightly increases the final baryon asymmetry. To summarize, we have established an intriguing correlation among GUT baryogenesis, DM phenomenology and neutrino mass mechanism, where the existence of DM revives GUT baryogenesis and induces the radiative neutrino mass.

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