Relativistic Modeling for the Giant Atom as a Key for Physics of Self Replication

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Abstract In this paper we put the relativistic basis for the giant atom like system. Before we go with the discussion we have to stress on that it may appear in the beginning of this long study that there was a contradiction with stable facts like the constant speed of light and like quantum physics but as soon as possible we would find that the study completely respects such facts. Also we have to remember all over this study that the final macroscopic state of the micro-scoping events inside the giant charge is the zero energy except from a little cut.

Keywords Giant Atom, Zero Energy, Quantum Physics, Self-replication

1. Introduction

From the relativistic relation \( m^2 = m_0^2 / 1 - \beta^2 \) where \( \beta = V/c \), if the speed \( V \) of a particle = \( c \) then the relativistic mass \( m \) would be infinite and if \( V^2 = 2c^2 \) then, \( m^2 = -m_0^2 \). Both are refused [1].

The Einstein famous equation [2] of the rest mass of a subatomic particle like a proton (or neutron…) is defined by;

\[
\left( \frac{k e^2}{r_o} \right) = m_o c^2 .
\]

Where it is a positive energy expresses about the inertial \( E_o \) such that \( m = m_o \). If we multiply the left side (where \( k \) denotes the electrostatic constant \( = 8.98 \times 10^9 N.m^2/c^2 \) and \( e \) is the value of the elementary charge in coulomb) by one then the right side should be typically the same (kindly look at the appendix number 1) as;

\[
\left( \frac{k e^2}{r_o} \right) \left[ \frac{r_o}{r} \right] = m_o c^2 .
\]

Where it is a positive inertial \( E_o \) not else and \( m = m_o \) (no motion). On the same form if we defined a system formed of a quantity of protons \( p \), distributed homogeneously among much more number of neutrons \( n \), such that \( n/p \) is defined (neglect quantum mechanics for a moment) and if we defined the quantity;

\[
\left( \frac{k e^2}{r_o} \right) \left[ \frac{r_o}{r} \right] = m_o c^2 \quad (1)
\]

Where \( m = m_o + 0 = m_o \) (If -and only if- the products inside the big brackets = 1). But actually we can write eq.1 in the form of the kinetic energy \( \Delta m c^2 = k e^2 p/r \) which when put with eq.1 we get; \( \Delta m c^2 = m_o c^2 \) which means that each defined proton of the sphere have gained \( \Delta E = m_o c^2 \) or literally each a proton have produced another one which is equivalent to; \( \Delta m c^2 = m_o c^2 \) which finally means that the inertial particle gained speed = \( c \) which is -in relativity-refused and so eq.1 becomes nonsense except it carries information that it can produce particles by a vague process. Now to overcome the problem in this refused equation and to initiate the action of physics of the sphere let the speed \( V \) of its particles be close to \( c \) so let us define \( V \) when extremely approaches \( c \) (but not equal \( c \)) as;

\[
V^2 = c^2 - c^2 \left( \frac{n}{p \times 1.29 \times 10^{36}} \right),
\]

where \( n/p \) is a constant equal the ratio of the number of the neutrons to that of the proton in our sphere.

Let; \( \beta^2 = V^2/c^2 \) and let;

\[
1 - \beta^2 = 1 - 1 + \left( \frac{n}{p \times 1.29 \times 10^{36}} \right) = \frac{n}{p \times 1.29 \times 10^{36}} = \frac{n}{p. \mu}
\]

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\[ m^2 = c_o(m_o)^2 = \mu \frac{p}{n} m_o^2 = \left(1.29 \times 10^{36} \times \frac{p}{n}\right) m_o^2 \] (2)

In the same sphere if each nucleon had such high speed (due to the relative positions = \( r_c \)) then the gravitational potential energy as speed function \( u_g(v) \) –from side of view of relativity for an imagined person localized at the centre of the sphere where he realizes the microscopic motive events - would be affected by the quantum speed \( V \) more than the electric potential of each a proton \( u_e(v) \) such that \( 1/c_o^{1/2} \)

\[ = \left[1 - \left(\frac{V^2}{c^2}\right)\right]^{1/2} \text{ would appear in the denominator of}\]

\( u_g(v) \) with power \( 3/2 \) while it appears in the denominator of \( u_e(v) \) only with power \( 1/2 \).

\[ u_g(v) = -Gn(m_o^2 c_o)(c_o^{1/2}/r_c). \text{ While,}\]

\[ u_e(v) = k e^2 p(c_o^{1/2}/r_c). \text{ Where; } r_c \text{ is the radius of the sphere in a rest form.}\]

\[
\left(\frac{k e^2}{r_o}\right)\left[\frac{r_o}{r_c} \cdot \frac{p}{n} \left(\frac{n}{p}\right)^{1/3}\right] = \left[-Gc_o \frac{m_o^2}{r_o}\right] \left[\frac{r_o}{r_c}\right]^{1/2} \] (3)

Where; \( c_o \) is the equality factor (defined from equation 2) and the negative sign means that the two sides act opposite to each other. The solution is in the form of asymmetric addition as;

\[ A + -A = 0 \] (4)

Let us search in other solution and so go back again;

\[ E_o = \left(\frac{k e^2}{r_o}\right) = m_o c^2 \text{ is an inertial positive rest energy. And}\]

\[
\left(\frac{k e^2}{r_o}\right) = \left(\frac{k e^2}{r_o}\right)\left[\frac{r_o}{r_c} \cdot \frac{p}{n} \left(\frac{n}{p}\right)^{1/3}\right] \text{ is refused.} \] (5)

Let us recall the equality \( (ke^2/r_o)\left[\frac{r_o}{r_c} \cdot \frac{p}{n} \left(\frac{n}{p}\right)^{1/3}\right] = -Gc_o m_o^2 n/r_s\)

Put \((-m^2)\) as a relativistic equivalent to \( m_o^2 \) and substitute in the last form of the equality as;

\[ (-m^2) = m_o^2 \]

\[ -Gc_o (-m^2 n)/r_s = \left(\frac{k e^2}{r_o}\right)\left[\frac{r_o}{r_c} \cdot \frac{p}{n} \left(\frac{n}{p}\right)^{1/3}\right] \] (6)

\[ -Gc_o (m_o^2 n)/r_s = - \left(\frac{k e^2}{r_o}\right) \] (1)

\[ Gc_o (m_o^2 n)/r_s = \left(\frac{k e^2}{r_o}\right) [1] = \left(\frac{k e^2}{r_o}\right) = m_o c^2. \] (7)

The middle side –like the left- has become positive energy; such that each side is –now- having the same magnitude and the same positive form \( 0; \left(\frac{k e^2}{r_o}\right) \). The equality has –now- symmetric additive solution as;

\[ u = m_o c^2 + m_o c^2 = 2m_o c^2 = m_o 2c^2 \] (8)

This final solution says that each of the three sides of eq.7 is not actually potential (not to bind the particles together) but explicitly an inertial energy where the sphere is particles factory. The equality \((-m^2 = m_o^2)\) has a relativistic solution in the form of;

\[ m^2 = m_o^2/1 - \beta^2 = m_o^2/1 - 2 = -m_o^2 \] (9)

Which gives a relativistic solution as; \( V^2 = 2c^2 \) (10)

This is the condition required for existence of the giant charge (or generally for the productive function) where such state does not mean \( V > c \) but definitely means particles production. And the defined continuous production of the particles (as we will see) guarantees firstly that \( m^2 = m_o^2 \) such that equation 2 would have the meaning of multiplication of the particles number by the factor \( c_o \) instead of increase the mass of the particle by the same factor where we are in a rest state (except from little residual energy as we will see) and secondly that the speed \( c \) is a universal constant. This means that the additive relation of \( V^2 = c^2 + c^2 \) (of eq.10) should be understood through the concept of eq.8 (concept of production of two particles added to each particle) and the negative of \( m^2 \) does not mean direction but it is an operator has a radical physical meaning such that it converted the kinetic electric and gravitational energies in the above equality into inertial energy. The same equality–after understanding its negative sign- leaves behind the meaning;

\[ m^2 = m_o^2 \text{ (and consequently } r = r_o) \] (11)

(That is if only –and only if- the two potentials of eq.1 are equal). And the equality of eq.11 explains the equality of eq.10 where each means that the sphere is in rest motion and the speed which appears is the inertial \( c \) of the produced particles. Now if we recall the refused equality in eq.1 and conclude it from eq.8 and 9 then it would become;

\[
\left(\frac{k e^2}{r_o}\right)\left[\frac{r_o}{r_c} \cdot \frac{p}{n} \left(\frac{n}{p}\right)^{1/3}\right] = 2m_o c^2/2 = m_o c^2 \]

(The left side of this equality when put as a pair like the relations in equations 7 and 8 gives with its conjugate the output;

\[ u \approx m_o c^2 + m_o c^2 \approx 2m_o c^2 \] (12)

These approximate relations because of the speed of a particle never equal \( c \) but may be \( v \approx c \). So let us again expect
speed \( v \) in the form;

\[
V^2 = c^2 - c^2/c_o = c^2 - c^2\left(\frac{n}{p \times 1.29 \times 10^{36}}\right)
\]

And let us put the relativistic mass as; \( m^2 = m_0^2/1 - \beta^2 \) such that \( \beta^2 = V^2/c^2 \) and \( 1 - \beta^2 = 1/c_o = 1 - 1 + \left(\frac{n}{p \times 1.29 \times 10^{36}}\right) = \left(\frac{1}{p \times 1.29 \times 10^{36}}\right) \)

Giving; \( m^2 = \left(1.29 \times 10^{36} \frac{p}{n}\right) m_0^2 \). So we have to modify the relation of \( V^2 = 2c^2 \) of the pair conjugate of eq.7 into \( V^2 \approx 2c^2 \) or

\[
V^2 = 2 \left[ c^2 - \left(\frac{c^2 \left(\frac{n}{p \times 1.29 \times 10^{36}}\right)}{n \times 1.29 \times 10^{36}}\right) \right] \approx 2c^2
\]

The equality of eq.11 would give the approximate relation; \( m^2 \approx m_0^2 \). The factor \( c_o \) which appears in the equality of eq.7 appears as the alternative relativistic solution (instead of \( m^2 = 1.29 \times 10^{36} \frac{p}{n} m_0^2 \)) under the pressure of the following realized facts; first \( m \approx m_0 \) and second the necessary equality of the two potentials (or precisely; the two inertial) of eq.7. This means that; the gravitational constant appears as; in the form of eq. 6 if and only if \( u_G \) has the meaning of inertia or explicitly; the triple \( u_G \) , \( u_e \) and \( u_n \) (\( u_G \) is the quantum term as we will see soon) all are one thing called \( m_o c_o^2 \).

The quantity \( m^2 \) of the function \( m^2_V = m_o^2 \) is conserved as;

\[
m^2_V = \mu m_o^2 = C_o(V)m_o^2 \frac{n}{p} = m_o^2 \frac{N}{p}. \text{ where;}
\]

\[
V^2 = 2 \left[ c^2 - \left(\frac{c^2 \left(\frac{n}{p \times 1.29 \times 10^{36}}\right)}{n \times 1.29 \times 10^{36}}\right) \right] \approx 2c^2
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\[
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\]

The density \( \mu \) of the number \( n \) appears from;

\[
\mu = c_o \left(\frac{n}{p}\right) = (c_o n)/p = \frac{N}{p}. \text{ Or explicitly;}
\]

\[
\mu = c_o (n(t,x)) / p(t,x) = N / p(t,x)
\]

This density allows us to use a new expression as Compton sphere instead of Fermi one. In GCU and because of \( n \gg p \) Pauli term of Compton sphere appears as predominant kinetic energy. For each neutron we have the average \( u_n =
\]

\[
\frac{u_n (A - 2Z^2)}{A} = u_n (n - 2p)/n = u_c
\]

In Compton sphere; Pauli Exclusion Principle needs to multiply the number of the filled states by two (+/– spin) and to divide over eight [5] to get only the positive space octant (where \( \sin -kx = \sin kx \) so we have;

The density \( N_e / V = 1/V_e = n / V \)

\[
u_n = (h^2 / 2m)(3\pi^2 N/V)^2/3.
\]

For all neutrons,
\[
= \int u_c \, dN = \frac{h^2}{2m} \left( \frac{3 \pi^2 \hbar^2}{5} \right)^{2/3} \int (\bar{N})^{2/3} \, dN = (3/5) u_c N.\]

Finally the average 
\[
< u_c > = (3/5) u_c. \]

By putting \( r_c \approx 2 \times 10^{-16} m \) and substitution we can estimate the average 
\[
< u_c > \approx 1.5 \times 10^{-10} j = m_o c^2 \tag{16}
\]

The relativistic gravitational potential \( u_g(V) \) (as speed function) would be affected by \( v \) more than the quantum term field \( u_c(V) \) such that \( 1/c_o = [1 - (V^2/c^2)] \) would appear in the denominator of \( u_g(V) \) with power 3/2 while it appears in the denominator of \( u_c(V) \) only with power 1/2.

\[
u_c \text{ would appear as;}
\]
\[
u_c = An^{2/3} \frac{c_o}{r_c^2 m_o c_o^{1/2}}
\]

And, \( u_o = -Br^{2/3} m_o c_o^{1/2} r_o \)

Where, \( A \) and \( B \) are constants and \( r_o = r_c \).

On equality – at the speed \( V \) approaches \( c \) - and putting \( m_o^2 = -m^2 \) we have the equality;

\[
\left(An^{2/3} / r_c^2 m_o\right) = Bn^{2/3} m_o c_o / r_o.
\tag{17}
\]

And from equation (16) we get;

\[
\left(An^{2/3} / r_c^2 m_o\right) = Bn^{2/3} m_o c_o / r_o = mc^2.
\tag{18}
\]

And by adding the two inertia;

\[
u = mc^2 + mc^2 = 2mc^2
\tag{19}
\]

Which realizes the state \( V^2 = 2c^2 \) as a relativistic solution for;

\[
m_o^2 = -m^2 \text{ where the negative sign gives the same radical physical meaning such that it is the operator which with this defined \( V^2 \) or definitely with this defined density. The equality of equation 18 could be written as;
\]

\[
An = B(nc_o)m^2 r \text{ where it shows the side of view of a person such that he sees only the macroscopic event and so he understands the radius of the sphere \( r \) from the side of view of the macroscopic reproductive function (under reference frame transformation) as; \( nc_o = N \).}
\]

Now we can notice that the constant in-between distance;

\[
(r_c = 2 \times 10^{-16} m) \text{ compelled each of the kinetics } u_c \text{ and } u_o \text{ to behave as inertial rest energy. Again like what we did in the potential (inertial) well of the proton we do also here.}
\]

So the modification is to avoid the refused solution of \( V = c \). So put \( r_c = 2 \times 10^{-16} m + \Delta r \) to obtain \( V^2 = 2 \left[ c^2 - \left( c^2 / \left( p / p_{1.29 \times 10^{36}} \right) \right) \right] \approx 2c^2 \). So in all above we have (instead of the equality) to put the approximate equality (=). You can notice that the global strategy of our manipulation is that we began with a speed \( v = c \) the we modified it to \( v \approx c \) then we put more modification as a defined \( v \) as; \( V^2 = c^2 - \left( c^2 / \left( p / p_{1.29 \times 10^{36}} \right) \right) \) and then instead of saying that \( V \) is close to \( c \) we say that; the in-between distance is close to \( r_c \) as a state of existence or actually as Gods state. On other words up till now we do not study how to get such high speed or such close distance but we say that if such a state is exist then what is its physics. In separate chapters we will find that actually such state had existence in a stage of stages of evolution of the solar system where it left behind many of parameters in the solar system as documents for this proposal. The final modification is to say that – instead of the above- all these microscopic events are initiating by the idea that; we may have a particle with cut energy in the form of;

\[
(m_o c^2 - \Delta m_o c^2).
\]

The neutron (like the proton) appears in its potential (or precisely, the inertial) well as a pair of conjugate. Here we have to notice that the state of the speed approaches \( c \) is a description of production of one single \( u \) of the pair while \( V^2 = 2c^2 \) is a description of the two \( u \) of the pair. We have also to notice that the protons have the same wavy behavior and so it has - also- \( u_c \).

But this term could be neglected because of the distance between two neighbor protons is \( = 10^{-16} r_c \) (where \( n/p \) as we will see is about ten powers twelve). Any way this term can appear (although it is comparatively small) during estimating \( p \), of GCU as;

\[
m_o c^2 = ke^2 q/r. \quad \text{where; } q(1 - 10^{-4}) = p = q.
\]

The average \( u \) inside Compton sphere and the factor 5/3; We estimated the average \( u_c \) \( = 1.5 \times 10^{-10} j = mc^2 \). From equation 3, the average \( u_e \) and the average \( u_e \) is;

\[
< u_c >= < u_e >= (3 / 5) m_o c^2
\]

This form is not compatible with the inertial form \( m_o c^2 \).

So we have to think in a manipulation returns the equations after integration to the general inertial form.

\[
\left( \frac{\left( ke^2 \right) r_o}{r_c} \right) \frac{p^{2/3} \, dp}{\left( \frac{n}{p} \right)^{1/3}} \quad \text{= } \quad Gc_o \frac{m^2}{r_o \cdot r_c} n^{2/3} \, dp
\]

Put the big brackets of the left and right sides to equal \( A \) and \( B \) respectively;

\[
\frac{A}{\left( \frac{n}{p} \right)^{1/3}} \int p^{2/3} \, dp = B \left( \frac{n}{p} \right)^{2/3} \, dp
\]

\[
= B \left( \frac{n}{p} \right)^{2/3} \int p^{2/3} \, dp
\]

\[
A \int p^{2/3} \, dp = B \left( \frac{n}{p} \right) \int p^{2/3} \, dp
\]

\[
\frac{A}{\left( \frac{n}{p} \right)^{1/3}} \int p^{2/3} \, dp = B \left( \frac{n}{p} \right)^{2/3} \, dp
\]

\[
= B \left( \frac{n}{p} \right)^{2/3} \int p^{2/3} \, dp
\]

\[
A \int p^{2/3} \, dp = B \left( \frac{n}{p} \right) \int p^{2/3} \, dp
\]
Now in the next stage (sphere $S_3$) we would have $\frac{n}{p}$ neutrons. In the next stage (sphere $S_2$) each particle appeared as; the original one and the added two as; $S_2 = 3S_1$. Before we go on we can put the general idea of the physical growth;

- The energy is quantized as $m_e c^2$
- The proton potential well is replaced by proton inertial well in which the energy is expressed as addition of protons.
- For each added proton there would be in the neutron inertial well (from the above equality) addition of $\frac{n}{p}$ number of neutrons so the added particles are multiples of huge proton (one proton $\frac{n}{p}$ neutrons).

Now in the next stage ($S_2$) we would have; $U_e$ per each mother proton $= \left( k \frac{e^2}{r_o} \right) \left( \frac{r_o}{r_e} \left( \frac{n}{p} \right)^{2/3} \right) \left( \frac{3}{5} \right)^{2/3} = \left( 2.08 \right) m_e c^2$

(you have to notice that the added fraction would disappear on collecting all over p; so for simplification let us say that; $U_e$ for each proton $= (2) m_e c^2$.

This means; each proton of $S_1$ would become 3 and then in a next stage would become 3x2 protons. And since from the above equality each proton is preserved by $\frac{n}{p}$ neutrons so the added neutrons in this stage (for each added proton) are;

$\left( \frac{3}{5} \right)^{2/3} \frac{n}{p} = 2 \frac{n}{p}$ neutrons (or you can see it as two neutrons are produced from each neutron). This means that;

Number of the particles of $S_3 = 6.08$ times that of $S_1$ or 2.08 times $S_2$.

And so on; each stage would use the output of the previous stage as its own input. The important notice here is to know how to compare between what occurs in the state of the unit giant charge (where we have electric energy per elementary charge equal $E_e$ which is equivalently conjugated with the relativistic gravitational energy per the same elementary charge $E_G$ and we have also due to the uncertainty -Pauli exclusion factor- energy per a neutron equal $E_u$ which is conjugated equivalently with the relativistic gravitational energy per the same neutron $E_{G2}$ where $E_{G1} = E_e = E_u = E_{G2}$ and what occurs in physics of the state of the growing giant charge where although the sphere adds particles yet the density $N/v$ is still conserved so we have the growing conjugate $E_e = E_{G1}$ and we have the constant conjugate $E_u = E_{G2}$. This is because the relativistic can realize the relative motions.

Now we can deduce that the giant charge is a little dark compact body -with a defined density- which although has great energy yet this energy is converted into fermions. This is why it does not degenerate further; because of at the range of Compton wavelength the relativistic gravitational energy ($E_G$) and its conjugates are transformed into fermions (repetition).

The binding energy (the cut energy);

You cannot remove all the energy from a system. Heisenberg said[6].

Actually in our system $\Delta E$ appears as $\Delta m c^2$.

We showed that our system respected the universal constant c and made the particles move with $V \approx c$. And then overcame the huge energy which had to be produced in such high speed such that the state $V^2 \approx 2c^2$ had guaranteed that the alternative solution for this energy is the production of multiples of the inertial $mc^2$. But this does not mean that we have zero binding energy.

The relation; $V^2 = 2 \left[ c^2 - \left( \frac{n}{px \cdot 1.29 \times 10^{36}} \right) \right]$ guaranteed that the subatomic particle which has $E_{G2} = m_e c^2$ (as a single particle outside our system) would have inside our
system (as produced particle) inertial energy \( E_o \)
\[
= m_o \left[ c^2 - \left( \frac{c^2}{p \times 129 \times 10^{36}} \right)^n \right]
\]
and so we would have a cut of energy as; \( \Delta E \)
\[
= \Delta mc^2 = m_o \left( c^2 \frac{n}{p \times 129 \times 10^{36}} \right) = m_o c^2/c_o = u_g/c_o = u_g
\]
(such that \( u_g \) is the ordinary gravitational potential without \( c_o \)). This term which appears in our system resembles the volume term \( a_o \) of the liquid drop model (semi empirical mass formula) [7] of the ordinary nucleus. So we have potential binding energy as;
\[
U_p = \Delta mc^2 + \theta + 0 + \ldots
\]
Actually this is the macroscopic equation which summarizes all the previous microscopic events where all the energies had appeared as particles production except a cut in the form of;
\[
\Delta mc^2 = m_o \left( c^2 \frac{n}{p \times 129 \times 10^{36}} \right) = m_o c^2/c_o = u_g \quad \text{which appears in this complete dark and rest sphere.}
\]
But we have to notice that this \( \Delta mc^2 \) is a cut from each of the produced particles and not from the mother one. Such a notice would give a respective consideration when we speak about a generation close to the mother sphere while would be inconsiderable with the far ones.

Defining the giant atom [8];
The giant charge \( A \) with radius \( r \) to orbit another one \((-A = B)\) with a radius of orbit \( R \) needs the following condition;

Since the particles of \( A \) (or \( B \)) are bind with each other by the average \( E_b \) per a huge charge;
\[
E_b = \frac{3}{5} \left( \frac{m.m}{r} \right) \left( \frac{n}{p} \right) \left( m \right)
\]
\[\text{(23)}\]
And since a huge charge \( e \) (such that each huge charge contains one elementary particle) of \( A \) to orbit \( B \) would have kinetic energy due to the mutual potential energy between \( e \) (the quantity of the charge in a huge charge) and \( p \) (number of the charges) of the sphere \( B \);
\[
E_k = \frac{1}{2} k \frac{e^2}{R} e
\]
\[\text{(24)}\]
When \( A \) (as one body; not each charge alone) orbits \( B \) (kindly look at appendix 2) it would be defined by;
\[
\frac{3}{5} \left( \frac{m.n}{r} \right) \left( \frac{n}{p} \right) \left( m \right) dp \geq \frac{1}{2} k \frac{e^2}{R} e dp
\]
\[\text{(25)}\]
\[
\frac{3}{5} \left( \frac{m.n}{r} \right) \left( \frac{n}{p} \right) \left( m \right) dp \geq \frac{1}{2} k \frac{e^2}{R} e dp
\]
\[\text{(26)}\]
\[
\frac{3}{5} \left( \frac{m.n}{r} \right) \left( \frac{n}{p} \right) \left( m \right) dp \geq \frac{1}{2} k \frac{e^2}{R} e dp
\]
\[\text{(27)}\]
If \( n/p \) was constant then;
\[
\frac{3}{5} \left( \frac{m.n}{r} \right)^2 \geq \frac{1}{4} k(e.p) \frac{e^2}{R}
\]
In our previous papers; the first named the giant atom like system and the second named the electrostatic energy in a rest form we took the solution of the equality such that the strategy of the giant atom is based on the least possible quantity of particles [8,9]
\[\text{(28)}\]
\[\text{(29)}\]
\[
\frac{n}{p} = 1.15 \times 10^{12}. \tag{30}
\]

And finally from eq. 14 and 30 we can estimate the constant;
\[
c_o = 1.29 \times 10^{36}/1.15 \times 10^{12} = 1.08 \times 10^{24}. \tag{31}
\]

The idea of the state \( V^2 = 2c^2 \) as a synonymous for particles production such that the daughter one has the same inertial mass of the mother one or \( m = m_o \) makes us go far to give a physical relativistic simulation for self-replication. \( V = c \)

Replication of the giant neutron unit

Here let us now remember that a macroscopic state in the form of \( V^2 = 2c^2 \) and equality in the form of equation 16 are required with a microscopic event defining the speed \( V \approx c \). Each of these three conditions has its role as follows;

The state (\( V^2 = 2c^2 \)) gives the meaning of production by copy and paste or in the relativistic expression it means \( mV^2 = -m_c^2. \)

Where the negative sign is vanished in the equality and consequently opens the way for the symmetric addition to realize the state; \( mV^2 = m_c^2 \) and also to realize the productive function as; \( mV^2 = 2mc^2. \). While the third condition would determine how many copies we would get or generally it defines the shape of this function.

We can summarize and say that; the state \( v \approx c \) as an odd state is the microstate which appears as motive inertial reference frame giving on the scope of special relativism slaw dilated time (the rest time multiplied by the equality factor \( c_o \)) where on this relativistic slaw time, the number of the particles \( N \) appears as; \( N = n \cdot c_o \). The other face of the coin is the rest reference frame (\( v^2 = 2c^2 \)) which appears as the even or the conjugate rest state where this rest time translates the state; \( v^2 = 2c^2 \) into two particles.

Let the neutrons of the giant neutron unit get in a contact state (Gods state) defined by \( r = r_c \) which gives from equations 15 (where you notice that \( r^2 \) appears in the denominator of \( u_c \)) and 16 (where \( c^2 \) appears);

\[
u_c = 1.5 \times 10^{-10} = mc^2. \]

And again we recall all the scientific relativistic basis of the microscopic events to get the equality with \( u_c \) and then the symmetric addition as;

\[
u_c + u_c = mc^2 + mc^2 = m2c^2 \]

which realizes the state \( V^2 = 2c^2 \). Or in the form of;

\[
u_c + u_c = mc^2 + mc^2 = 2(mc^2) \]

which means two neutrons are added to the mother one.

Suppose we have two neutrons near to each other such that each of the relativistic and the quantum wavy effect is considerable. Put;

\[
\beta^2 = \frac{v^2}{c^2} \quad \text{and} \quad 1/(1 - \beta^2) = \mu \tag{32}
\]

The quantum behavior appears as;

\[
p \lambda = h
\]

Putting \( r_c = 2 \times 10^{-16} \) meter and \( m = 1.66 \times 10^{-27} \) kilogram;

From above and from (33); \( V = c \)

From equation 16 put \( E_c = m_o c^2 \) and the equality needs;

\[
m_o c^2 = Gm_o^2 \mu / r_c \tag{33}
\]

\[\therefore \mu = 1.6 \times 10^{38} \tag{34}\]

For a population of neutrons \( n \) with the same density we would have

\[
E_c.n = nm_o c^2 = \frac{2}{5} m^2(n_c) n^{2/3} / r_c \tag{35}
\]

Here you see the term \( n.c_o \) appears as a conjugate and so it looks like the modified form of equation (20). And also you notice that \( m \) appeared versus \( m_o \) while the alternative relativistic solution appears as multiplication of \( n \) by the speed function factor \( c_o(v) \).

\[\therefore 3/5 c_o n^{2/3} = \mu = 1.6 \times 10^{38} \]

\[c_o = 2.8 \times 10^{38}/n^{2/3} \tag{36}\]

You can see \( c_o \) of the reproductive function differs in the form from that of GCU and it depends on the arbitrary variable \( n^{2/3} \).

Now to realize the equality of equation 35 put the speed of \( u_c = V_c \) in a form like eq.2 as;

\[(V_c)^2 \approx c^2 = c^2 - c^2 / c_o \]

The global solution is formed of;

1- \( m = m_o \)

2- \( N = 2n \) (at infinitesimal \( \Delta t \)). This occurs by putting \( V^2 \approx c^2 \) where the output appears as duplication of the giant neutron unit.

3- \( N_g = c_o n \) (at \( \sum \Delta t \) ). The output appears as the continuous growth of the unit throughout the time.

Of course the cut term which appears after the minus in eq.37 allows a binding energy in the form of \( mc^2/c_o \) per a produced particle which can take the form of; \( E_g.c_o/c_o = E_g \).

Can we create a reproductive function of the giant neutron unit?

Of course we cannot bring particles with in-between distance = \( u_c \) and it is not easy to bring them in the density of the reproductive function. So it may be formed by recalling the corresponding circumstances. So let us bring neutrons such that their average speed equals the average speed of the particles of the reproductive function as \( V^2 = c^2 / c_o \). And if we have number of neutrons equal about \( 10^{21} \) which gives \( n^{2/3} = 10^{14} \).

And then; \( c_o \) of the reproductive function = \( 2.8 \times 10^{38}/10^{14} = 2.8 \times 10^{24} \).

\[\therefore V = \sqrt{(c^2/c_o)} \approx 3.5 \times 10^{-8} m/s. \]

From de Broglie equation this speed gives; \( r \approx 0.0002 m \).

So if we could to collect this quantity of neutrons in a defined evacuated volume such that \( R = 0.0002 \times n^{1/3} \) then I suggest that the collection would appear as reproductive function and the particles would get (by
correspondence principle and not by gradual approach) the simultaneous state of \( r = 2 \times 10^{-16} \) meter. It is easy to conclude that \( R \) is n-independent such that; \( R = 2000 \) meter.

2. Conclusions

Physics of the giant atom like system is a scientific truth. This is confirmed by that we found complete coincidence between the parameters of such a system with that of the solar system.

The scientific value of this mathematic study is that it discovers the relativistic basic relation between the two long range acting forces and the inertial mass. Explicitly we can say that; each of the relativistic gravitational and the electrostatic energy can appear as inertial energy in the form of \( m_{\circ}c^2 \) minus a little cut in the form of \( \frac{e^2}{c_0^2} \) which realizes the reproductive function and describes physics of the giant atom.

Our study put also a suggestion for how to create a reproductive function.

Appendix 1

One may doubt and say that \( \Delta E \) is not equal \( \left( \frac{e^2}{r_0} \right) \) but it has the form of;

\[
\Delta E = \frac{1}{2} \left( \frac{e^2}{r_0} \right) \] [1] = \frac{1}{2} m_o c^2.

Never mind. let us go on to estimate \( \Delta E \). Actually Lorentz postulated that the energy of the charged particle is due to its electromagnetic behavior. So let us estimate the part of the energy due to the electric field and add it to that part due to the motion (spin) of the charged particle (magnetic energy). Now in each infinitesimal volume we have the electric energy density;

\[
\Delta E = \frac{1}{2} \frac{e^2}{r_0}
\]

Where \( \omega \) is the permitivity constant of space and \( (E.E) \) is the dot product of the electric field vector (the result is scalar). And all over the spherical volume we have the electric potential per particle;

\[
\Delta E = \frac{e^2}{2 \pi \mu_0 c^4} \int \int \int r^2 \sin \theta \; dr \; d\theta \; d\phi = \frac{e^2}{2 \pi \mu_0 (2a)} = \frac{1}{2} m_o c^2.
\]

The magnetic part of the energy due to spin;

We would estimate the magnetic field \( B \) in z- direction (in S.I. units) postulating a literal circular motion of the charged particle with radius of rotation equals its classic radius \( a = r \). This postulated motion is coincident with the method by which we estimated the electric part of the energy otherwise you cannot doubt in equation1). So we would estimate the magnitude of \( B \) in z- direction due to motion of the charged elementary particle in a circle with length \( l = 2\pi a \) where \( a = r \). From Biot-Savart law; \( B = \frac{\mu}{4\pi} \left[ \frac{dl}{a^2} = \frac{\mu I}{2r} \right] \) where \( \mu \) is the permeability constant of the space and \( i \) is the electric current of the charged particle as;

\[
i = \frac{e^v}{2\pi a} \Rightarrow B = \frac{4\pi e}{4\pi a c^2}. \] The magnetic moment \( m \) is estimated as;

\[
m = i n a^2 \]

\[
\therefore \text{The energy part due to spin};
\]

\[
u = m \times B \text{ where } \times \text{ is the cross product which gives in z- direction};
\]

\[
= \frac{e^2}{4\pi a c^2} \mu.
\]

Put \( v = c \) and put \( \omega \mu c^2 = 1 \)

\[
\therefore \Delta \mu = \frac{e^2}{4\pi a c^2} \mu . \]

Or we can estimate it directly from Maxwell [10] equations as;

\[
(\Delta E)_2 = B^2 / 2 \mu. \text{ Put } B = -E/c, \text{ and } \omega \mu c^2 = 1
\]

\[
\therefore (\Delta E)_2 = E^2 / 2. \text{ And allover the volume gives the same above result.}
\]

And the total energy is estimated by adding the two types of energy as;

\[
\therefore \Delta E = 2 \frac{e^2}{4\pi a (2a)} = m_o c^2.
\]

Appendix 2

It is easy to understand that if the total gravitational binding energy between the elementary particles inside the sphere was just equal or more than the attractive total electric energy between the two spheres then the sphere \( A \) would orbit the sphere \( B \) as;

\[
\frac{3}{5} \left( \frac{m_1}{r} \right) \left( \frac{2}{p} \right) m. \text{ } p \geq \frac{1}{2} \frac{k n p}{r} e . p
\]

Actually this equation is not accurate and so we need the next discussion;

Let the amount of the elementary particles of the sphere \( A \) (the electrons) to be labeled \( p_i \) where \( i = 1, 2, 3, \ldots \ldots \).

And let the summation of the elementary particles of the sphere \( B \) (the protons) to equal \( P \), where \( P = p \).

If the last equation was not obeyed then the charges of the two spheres would be attracted to each other as elementary particles to form atoms.

On the first event when the first electron \( p_i \) attracted into the sphere \( B \), the attractive electric energy \( E \), would be proportional with \( P \).

On the second event when the second electron \( p_i \) attracted to \( B \), the electric energy would be proportional with \( (P - 1) \) because of the previous event have transformed one proton of \( B \) into atom. And so on each event would subtract a proton till we reach to the last event where the sphere \( B \) contains one proton only. Finally we would have the summation of the series as;

\[
\sum E = k (e . P/R)p / 2 = k (e/R)p \int dp
\]

Now we reached to the point that the two spheres to be
attracted toward each other (as spheres not as elementary particles) we need;

\[
\frac{3}{5} \left( \frac{m \cdot n}{r} \right) \left( \frac{n}{p \cdot m} \right) \cdot p \geq k(e/R) \int dp
\]

So the two spheres to orbit each other we need the form of equations 25 and 26.

The last notice here is that; actually the elementary particles of the sphere A are not pulled to the other sphere as singles but actually as shots; the superficial ones then the deeper but finally we can define the series;

\[
(P - a) + (p - b) + (p - c) \ldots \ldots c + b + a = \frac{p^2}{2}
\]

REFERENCES

[1] Albert Einestein (2001), Relativity; the special and general theory. Reprint of 1920 translation by Robert W. Lawson Ed.
[2] David J. Griffiths, Introduction to quantum mechanics, Prentice-hall, 1995, p 155.
[3] Alzergin and v. Korepin, Letter in mathematical physics, vol. 6, 1982.
[4] Garay Luis J, Quantum gravity of minimum length. International journal of modern physics (1995).
[5] Alan Doolittle, Density of states and Fermi energy concept.
[6] Werner Heisenberg, The physical principle of quantum theory.
[7] Bailey, D. Semi empirical nuclear mass formula: Strings and binding energy 2011.
[8] Eldieb Emad, The electrostatic energy in a rest form; evidences and recommendations, international research journal of pure and applied physics, vol. 3, No. 1 June. 2015.
[9] Eldieb Emad, The giant atom like system, advanced studies in theoretical physics vol. 3, 2009.
[10] Claus W. Turtur, An explanation of electron mass by the energy of its fields, university of applied sciences Braunchweig-Wolfenbuttel, Germany.