Effects of Synchrotron Cooling and Pair Production on Collisionless Relativistic Reconnection

Hayk Hakobyan1, Alexander Philippov2,3,4, and Anatoly Spitkovsky1

1 Department of Astrophysical Sciences, Peyton Hall, Princeton University, Princeton, NJ 08544, USA; hakobyan@astro.princeton.edu
2 Department of Astronomy, University of California, Berkeley, CA 94720-3411, USA
3 Center for Computational Astrophysics, Flatiron Institute, New York, NY 10010, USA

Received 2018 September 26; revised 2019 March 27; accepted 2019 April 12; published 2019 May 24

Abstract

High-energy radiation from nonthermal particles accelerated in relativistic magnetic reconnection is thought to be important in many astrophysical systems, ranging from blazar jets and black hole accretion disk coronae to pulsars and magnetar flares. The presence of a substantial density of high-energy photons (>MeV) in these systems can make two-photon pair production (γγ → e+ e−) an additional source of plasma particles and can affect the radiative properties of these objects. We present the results of novel particle-in-cell simulations that track both the radiated synchrotron photons and the created pairs, with which we study the evolution of a two-dimensional reconnecting current sheet in pair plasma. Synchrotron radiation from accelerated particles in the current sheet produces hot secondary pairs in the upstream, which are later advected into the current sheet where they are reaccelerated and produce more photons. In the optically thin regime, when most of the radiation is leaving the upstream unaffected, this process is self-regulating and depends only on the background magnetic field and the optical depth of photons to pair production. The extra plasma loading also affects the properties of reconnection. We study how the inflow of the secondary plasma, with multiplicities up to several hundred, reduces the effective magnetization of the plasma, suppressing the acceleration and thus decreasing the high-energy photon spectrum cutoff. This offers an explanation for the weak dependence of the observed gamma-ray cutoff in pulsars on the magnetic field at the light cylinder.

Key words: acceleration of particles – gamma rays: stars – magnetic reconnection – plasmas – pulsars: general – radiation mechanisms: non-thermal

1. Introduction

One of the key observational characteristics of γ-ray pulsars is a hard power-law spectrum (with a typical photon index Γ ≈ 1 − 2) extending to cutoff energies of a few GeV (Abdo et al. 2013). While pulsed radio emission is generated in the inner magnetosphere close to the neutron star surface, gamma radiation usually arrives in different rotational phases and based on its light-curve properties is thought to be produced mainly in the outer magnetosphere close to the Y-point (see, e.g., Bai & Spitkovsky 2010; Contopoulos & Kalapotharakos 2010; Harding & Kalapotharakos 2015). Reconnection in the current layer beyond the Y-point just outside the light cylinder is a plausible mechanism of nonthermal particle acceleration that can later form the observed spectrum via synchrotron radiation (Coroniti 1990; Lyubarskii 1996; Péri 2012; Cerutti et al. 2016; Philippov & Spitkovsky 2018).

However, while the light curves and spectral shapes of pulsar γ-ray emission can be naturally explained with the current sheet emission, there is a disagreement between the observations and the predictions of spectral cutoff of this model. The high-energy spectral cutoff in pulsars, as measured by the Fermi Observatory, depends weakly on the magnetic field at the light cylinder, BLC. As shown in Figure 1, for a wide range of BLC = 10^5–10^6 G the cutoff energy varies from 1 to around 6 GeV (Abdo et al. 2013). On the other hand, the model that incorporates reconnection predicts a stronger dependence. In relativistic reconnection, the magnetic energy that can be deposited into particle kinetic energy is controlled by the magnetization parameter at the light cylinder, σLC, defined as the ratio of the magnetic energy to plasma enthalpy. For the cold plasma this parameter is equal to

σLC ≈ BLC^2 / 4πnLCm_e c^2, \tag{1}

where BLC and nLC are the magnetic field and the plasma density near the light cylinder. In particular, in a strongly magnetized plasma, σLC ≫ 1, the particle spectrum cutoff does not typically exceed few times σLC (Sironi & Spitkovsky 2014; Werner et al. 2016). Note here that there are mechanisms that can increase this cutoff to much higher energies in the uncooled reconnection (Petropoulou & Sironi 2018). We will discuss later why this is not possible when strong synchrotron cooling is present.

The plasma loading along the separatrix to the light cylinder and outer magnetosphere is set by the multiplicity of the primary cascade near the polar cap, κ ≈ 10^4 (Daugherty & Harding 1982; Timokhin & Arons 2013; Timokhin & Harding 2019) and the local Goldreich–Julian density, nGJ ≈ ΩBLC/2πec (i.e., nLC ≈ κnGJ). The multiplicity of primary cascade, κ, is roughly insensitive to the magnetic field strength. This means that the plasma density scales linearly with the magnetic field at the light cylinder, and thus from formula (1) the maximum particle energy, γmax ~ σLC, also scales linearly with BLC. If these particles radiate synchrotron photons which form the observed γ-ray emission, the cutoff energy of photon spectrum, Eγcutoff, will correspond to the maximum energy of particle spectrum set by σLC. This will lead to a strong dependence of the cutoff energy on the
background magnetic field: $E_{\text{cutoff}} \propto \gamma^2_{\text{max}} B_{\text{LC}} \propto B_{\text{1L}}^{-2} P^2$, where $P$ is the period of the pulsar. Periods of $\gamma$-ray emitting normal pulsars vary within less than a decade; the same is true for $\gamma$-ray emitting millisecond pulsars. For simplicity, we will ignore the dependence on periods in our further discussion. We will comment in Section 5.3 on why this assumption is valid. This discrepancy with the observed weak dependency suggests that there must be a self-regulating source of additional mass loading of the current layer that effectively decreases the magnetization and suppresses the particle acceleration for higher magnetic fields.

In the region close to the current layer, the number density of high-energy synchrotron photons is sufficiently high for two-photon pair production to be efficient. This process has previously been studied in the context of outer gap acceleration models (Arons 1996; Takata et al. 2010). As was shown by Lyubarskii (1996) for the reconnection-powered acceleration occurring in the equatorial current sheet, this pair creation process can significantly increase the plasma population with multiplicities of secondary pairs up to several thousand ($\sim 3000$ for Crab). On the other hand, thermal keV radiation from the neutron star surface is insufficiently luminous to interact with high-energy GeV photons and significantly contribute to pair production. Thus the main effect is due to high-energy (keV to GeV) synchrotron photons emitted locally in the sheet interacting with each other in the current layer near the Y-point.

Since plasma loading of the reconnection layer affects the rate of reconnection and its acceleration properties, it is reasonable to expect that the system will reach a self-consistent steady state in both particle and radiation spectra. Such steady states driven by secondary pair plasma loading can also have observational manifestations in other environments where extreme reconnection with pair production is thought to occur, such as in blazar jets (Giannios et al. 2009), magnetar flares (Thompson 1994), or black hole disk coronae (Beloborodov 2017).

In this paper, we study the previously unexplored regime of reconnection with self-consistent pair production that achieves high multiplicities of secondary plasma. We present the results of relativistic particle-in-cell simulations of a two-dimensional reconnecting current sheet with photon radiation and pair production, where we create and track photons as separate particles and self-consistently incorporate two-photon pair production events. In Section 2 we revisit the general picture of relativistic magnetic reconnection and introduce the main parameters of the problem. We then discuss an analytical model of how pair production and secondary plasma loading affects the steady state of reconnection and, as a result, the emerging particle and photon spectra. In Section 3 we introduce the numerical setup that we used and describe our algorithm. In Section 4 we summarize the main results and discuss how they can be applied to understand the high-energy radiation from pulsars.

2. Reconnection with Pair Production: Theory

In this section we give a theoretical outline of our paper, as well as introduce the main terminology and current understanding of how relativistic reconnection works.

2.1. Relativistic Reconnection in $e^\pm$ Plasma

It is well known that a current layer separating uniform oppositely directed magnetic field regions is unstable. Plasmoid instability, developing quickly on Alfvén crossing timescales, initiates magnetic reconnection, breaking the current layer into a chain of outflowing plasmoids (see, e.g., Tajima & Shibata 1997; Loureiro et al. 2007). Energy of the magnetic field is liberated in this process, which in the relativistic case powers nonthermal particle acceleration, forming a power-law spectrum of particles with a cutoff set by the magnetization.

In Figure 2 we show a typical simulation snapshot of a two-dimensional current sheet undergoing the plasmoid instability and reconnection. All the important features, such as the plasmoids, plasmoid mergers, and secondary current sheets, are shown in the figure for guidance. The pattern of plasmoids is self-similar on a wide range of scales, and their evolution is stochastic: smallest plasmoids move along the layer with the Alfvén velocity (which in relativistic case is close to $c$), but they also merge to become larger and slower, with bulk motions that are just marginally relativistic (for more details see Sironi et al. 2016).

Between the plasmoids, the annihilated magnetic field in the $x$-points allows the reconnection electric field to accelerate particles. Along with the primary current layer, there are also secondary layers that occur during the plasmoid collisions, serving as additional locations of particle acceleration (Guo et al. 2015). Plasmoids advect hot plasma containing the most energetic particles along the sheet with the Alfvén velocity, while the cold upstream plasma, having typically small Lorentz-factors, $(\gamma) \approx 1$, inflows with a characteristic velocity $\beta_{\text{in}} \equiv v_{\text{in}} / c \sim 0.1–0.2$, which corresponds to the reconnection rate.

The main dimensionless parameter controlling the dynamics of collisionless relativistic reconnection is the cold magnetization parameter, $\sigma_c \equiv (B^2 / 4\pi n m_e c^2)$, that sets the available magnetic energy per particle. Here, $n$ is the pair plasma density far from the reconnection layer, where the unreconnected field has the value $B$. When $\sigma_c \gg 1$, the majority of particles accelerated in the current layer is typically in the ultrarelativistic regime. Magnetization controls the maximum energy to which a particle can be accelerated in reconnection. In particular, as was shown by Sironi & Spitkovsky (2014) and Werner et al. (2016), in the $x$-point particles can be accelerated...
up to a few times $\sigma_c$. The plasmoids can further accelerate particles, extending the power law to much higher energies (Zenitani & Hoshino 2001; Guo et al. 2016; Sironi et al. 2016; Petropoulou & Sironi 2018).

In pulsars, the value of magnetization, which depends both on the magnetic field strength and the plasma density, can be estimated from the spin-down power of the pulsar and the properties of the initial pair production cascade near the polar caps (Arons 1983; Lyubarsky 1995; Lyubarsky & Kirk 2001; Medin & Lai 2010; Timokhin 2010). Typically, this parameter lies between $10^2$ and $10^3$; for the Crab it can also be directly constrained from PWN observations to be close to $10^4$. This value sets the cutoff energies to which particles can be accelerated.

### 2.2. Particle Cooling and Photons

Both electrons and positrons are subject to radiation cooling at relativistic energies. In this paper we only consider synchrotron cooling, while inverse-Compton (IC) cooling may also be important in some contexts (Werner et al. 2019). If the synchrotron cooling time is shorter than the acceleration time (we call this a strong cooling regime), accelerated particles will quickly lose their gained energy in the large background magnetic field without having a chance to reaccelerate again. Unlike the case without cooling, the highest energy particles will no longer be located within the plasmoids, since the plasmoids have typically higher magnetic fields and the particles within them are efficiently cooled. Instead, most of the high-energy particles will be piled up in the vicinity of plasmoids and along the primary and secondary current layers where the magnetic field is close to zero; the maximum energy will thus no longer be set by the plasmoid sizes. Even when synchrotron cooling is strong, the energy particle cutoff will be close to a few times $\sigma_c m_e c^2$, as these particles would still accelerate in the primary and secondary current sheets where the local cooling is inefficient.

The cooling regime is parametrized by the value of the Lorentz factor of particles, $\gamma_{\text{rad}}$, for which the radiation drag force is comparable to the accelerating force (for the accelerating electric field, we assume $E \sim \beta_{\text{rec}} B_0$; hereafter, we use subscript “0” for upstream values),

$$2 \sigma_T \frac{B_0^2}{8\pi} \gamma_{\text{rad}}^2 = e \beta_{\text{rec}} B_0,$$

where $\beta_{\text{rec}} \approx 0.1$ is the steady-state reconnection rate, and $\sigma_T$ is the Thomson cross section.

The radiation from a single plasma particle is described by the synchrotron spectrum, peaking at frequency $\omega_{\text{syn}} \approx eB_0 \gamma_{\text{rad}}^2/m_e c$. An important benchmark energy for pair production is the electron (positron) rest-mass energy, $m_e c^2$, which determines the minimum center-of-momentum energies for two photons to pair produce. We are thus interested to know which plasma particles radiate photons with characteristic energies close to $m_e c^2$. This sets another dimensionless parameter—the Lorentz factor of these particles, $\gamma_c$, determined by

$$\hbar \frac{e B_0 \gamma_c^2}{m_e c} = m_e c^2.$$  \hspace{1cm} (3)

Combined together, the cold magnetization parameter of the upstream, $\sigma_c$, radiation-reaction limit, $\gamma_{\text{rad}}$, and the pair threshold parameter, $\gamma_c$, give the full description of the synchrotron-cooled reconnection problem. We can rewrite the definitions as

$$\gamma_{\text{rad}}^2 = \frac{3\beta_{\text{rec}} B_3}{2 B_0}, \quad \gamma_c^2 = \frac{\alpha B_3}{B_0} = \frac{B_S}{B_0},$$  \hspace{1cm} (4)

where $\alpha$ is the fine-structure constant, $1/137$, $B_3 = m_e^2 c^4 / e^3$ is the classical magnetic field, and $B_S = m_e^2 c^3 / e \hbar$ is the Schwinger field.

For a typical pulsar with the magnetic field at the light cylinder $B_0 = B_{1,LC} \sim 10^5$ G, we find

$$\gamma_{\text{rad}} \approx 10^4 \left( \frac{B_0}{10^5 \text{ G}} \right)^{-1/2}, \quad \gamma_c \approx 2 \cdot 10^4 \left( \frac{B_0}{10^5 \text{ G}} \right)^{-1/2}. \hspace{1cm} (5)$$

For the Crab, with $B_{1,LC} \sim 4 \times 10^6$ G, these values are $\gamma_{\text{rad}} \approx 10^4$ and $\gamma_c \approx 3 \times 10^3$ (Uzdensky & Spitkovsky 2014), and the typical magnetization near the light cylinder is $10^{-3} - 10^{-2}$. We, thus, have a hierarchy of energy scales with $\gamma_c \ll \gamma_{\text{rad}} \lesssim \sigma_c$, which we will use in our simulations.

### 2.3. Two-photon Pair Production

Two photons can interact through the Breit–Wheeler process to form an electron–positron pair, $\gamma \gamma \rightarrow e^+ e^-$ (Breit & Wheeler 1934). This can happen if the center-of-momentum energy of photons is greater than the rest-mass energy of the electron–positron pair

$$s \equiv \frac{1}{2} (\tfrac{1}{m_e c^2})^2 (1 - \cos \phi) > 1,$$  \hspace{1cm} (6)

where $\varepsilon_1$ and $\varepsilon_2$ are the lab frame photon energies, and $\phi$ is the angle between their momenta. The cross section for this
interaction behaves as $\sqrt{s - 1}$ near $s \geq 1$, peaks around $s \approx 2$, and drops down as $1/s$ for $s \gg 1$. In Figure 3 we show the magnitude of this cross section plotted versus the relative angle of two interacting photons, $\phi$, and the product of their energies measured in $m_e c^2$. White shaded region corresponds to values of $s$ where pair production is not possible.

Figure 3 demonstrates two important facts: the high-energy photons ($\varepsilon \gg m_e c^2$) pair produce preferentially with the lower energy ones ($\varepsilon \ll m_e c^2$), while the ones with intermediate energies ($\varepsilon \approx m_e c^2$) pair produce with each other. Also, the small angle interactions with $\phi \approx 0$ are suppressed, while the head-on collisions, $\phi \approx \pi$, are more preferred.

We will consider a system to be optically thin to two-photon pair production, $\tau_{\gamma \gamma} \ll 1$, if at all energies only a small fraction of photons is converted to pairs. This means that most of the photons stream freely out of the system without any interactions. Note also that this condition is hardest to satisfy for the highest energy photons, since they typically have a high pair production probability while streaming through a dense background of low-energy radiation.

In an optically thin regime for a power-law energy distribution of photons, one can show that photons in a wide range of energies contribute roughly equally to pair production. If the photon energy cutoff is at $\varepsilon_{\text{max}}$, all the photons from $\varepsilon_{\text{min}} \approx (m_e c^2)^2 / \varepsilon_{\text{max}}$ to $\varepsilon_{\text{max}}$ are equally important to consider. This makes the problem of photon tracking numerically challenging. On the other hand, very low-energy photons, $\varepsilon \ll \varepsilon_{\text{min}}$, have no high-energy partner to interact with, and can thus be thrown out of consideration in the context of pair production.

2.4. Steady State and the Effective Secondary Plasma Density

We now describe a simple model of reconnection with synchrotron cooling and pair production to better illustrate the pair loading feedback mechanism and the steady state. We also predict the steady-state multiplicity of secondary plasma in our simulations and in $\gamma$-ray pulsars, and it is dependence on the background magnetic field.

The general picture is schematically shown in Figure 4, where we show how different ingredients of reconnection work together to build up the feedback and ultimately drive the system to a steady state. Most of the plasma resides in the current sheet (blue region in Figure 4), where it gets accelerated and radiates a power-law distribution of photons $d\nu / d\varepsilon_{\gamma} \propto \varepsilon_{\gamma}^{-1}$. Each particle experiences a radiative drag force and loses its energy to radiation at the rate

$$\dot{\varepsilon} = 2\sigma_T c B_0^2 \gamma_{\text{rad}}^2 = e^2 \beta_{\text{sec}} B_0 \left( \frac{\gamma_{\gamma}}{\gamma_{\text{rad}}} \right)^2, \quad (7)$$

where $\gamma_{\text{rad}}$ is defined in Equation (2).

We will assume that each particle with energy $\gamma_0 m_e c^2$ radiates photons with synchrotron peak frequency in the fixed upstream field $B_0$,

$$\varepsilon_{\gamma} = m_e c^2 \left( \frac{\gamma_{\gamma}}{\gamma_0} \right)^2, \quad (8)$$

where $\gamma_0$ is defined in Equation (3). The radiated photons pair produce in the upstream, creating secondary pairs that feed the current sheet further. The total photon production rate can be found from Equations (7) and (8),

$$\dot{n}_\gamma \propto \varepsilon_{\gamma}^{-1} \int_{\varepsilon_{\text{min}}}^{\varepsilon_{\text{max}}} \varepsilon_{\gamma}^{-1} \varepsilon_{\gamma}^{-1} d\varepsilon_{\gamma} \propto \varepsilon_{\text{min}}^{-1} \propto \varepsilon_{\text{max}}^{-1}, \quad (9)$$

where we defined the multiplicity, $\eta$, as the ratio of the secondary plasma density to that of the primary, $n_{\text{sec}} / n_0$.

Given the spectrum of photons, we can find how the number of pair producing photons scales with the spectral cutoff

$$n_{\gamma} \propto \int_{\varepsilon_{\text{min}}}^{\varepsilon_{\text{max}}} \varepsilon_{\gamma}^{-1} \varepsilon_{\gamma}^{-1} d\varepsilon_{\gamma} \propto \varepsilon_{\text{min}}^{-1} \propto \varepsilon_{\text{max}}^{-1}, \quad (10)$$

where we used the fact, that $\varepsilon_{\text{min}} \varepsilon_{\text{max}} \approx (m_e c^2)^2$. 

---

**Figure 3.** Two-photon pair production cross section as a function of the angle between their momenta, $\phi$, and the product of photon energies in units of $m_e c^2$. The pair production probability is highest when the center-of-momentum energy is $\approx \sqrt{2} m_e c^2$. For small angles only the most energetic photons can pair produce with each other, while head-on interactions allow a wider range of energies.

**Figure 4.** Schematic illustration of the reconnecting current sheet in its steady state. Plasma in the current sheet cools down via synchrotron radiation. These photons later pair produce in the upstream, and secondary pairs are advected into the current sheet.
Photons of the highest energies are radiated by the particles with the highest Lorentz factors. Reconnection accelerates particles up to a few times $\sigma$, which is lower than the initial value $\sigma_0 = B_0^2/4\pi\rho_0 m_e c^2$ by a factor of $(1 + \eta)$. Thus, when the multiplicity grows, the effective magnetization and the maximum photon energy decrease, shrinking the energy band of pair producing photons (decreasing $\bar{n}_\gamma$). This is the pair production feedback that drives the system to a self-regulated steady state.

To estimate the steady-state multiplicity, we can write the pair production rate as follows:

$$n_\gamma = \eta n_0 \sigma \rho_0 / m_e c^2,$$

where the dimensionless parameter $f_0$ sets the interaction cross section, $\sigma_{\gamma} = f_0 \sigma_{\gamma T}$, and depends on the energies and momenta of interacting photons. The peak value of $f_0$ is close to 0.3; we will take an empirical value of 0.1. The final result depends weakly on this parameter.

In steady state, both the secondary plasma and the photons are advected out of the reconnection region. Our simplified model is purely one-dimensional: the system extends infinitely in the horizontal and out-of-plane directions in Figure 4, while the only variation appears in the direction perpendicular to the current sheet (vertical direction in the figure). We then introduce two length-scales in this direction in the current sheet inflow domain: $s_1$, the region where most of the photon radiation happens, and $s_2$, where most of the pair production events take place. We can then convert the production rates to steady-state densities:

$$n_\gamma = n_\gamma s_1 / c, \quad n_{sec} = n_{sec} s_2 / c.$$  

Combining Equations (9)–(12), we find

$$n_{sec} = n_0 \eta = \beta_{sec} f_0 \sigma_{\gamma T} e^2 B_0^2 \rho_0^2 \left( m_e c^2 \right)^2 \frac{\eta s_1}{s_2} \times (1 + \eta)^2 \left( \frac{\eta_{\text{max}}}{m_e c^2} \right)^{2\gamma - 2} \left( \frac{\gamma}{\gamma_{\text{rad}}} \right)^4,$$

where we set $\eta_\gamma = n_\gamma (\eta_{\text{max}} / m_e c^2)^{\gamma - 1}$. We can then take $\eta_{\text{max}} / m_e c^2 = (\sigma / \gamma_{\text{rad}})^2$, with $\sigma = \sigma_0 (1 + \eta)$, and substitute $n_0 = B_0^2 / 4\pi \sigma_0 m_e c^2$. After some simplification, we get

$$\eta \left( \frac{1 + \eta}{1 - \eta} \right)^{6 - 4\gamma} = \frac{\beta_{sec} f_0 \sigma_{\gamma T} e^2 B_0^2}{4\pi \left( m_e c^2 \right)^2} \frac{\eta_{\text{max}}}{\eta_{\text{rad}}} \frac{\sigma_0^2}{\gamma_{\text{rad}}},$$

(16)

To express this relation through dimensionless numbers, let us substitute $\sigma_{\gamma T}$ from (2) and define the cold plasma gyroradius as $\rho_0 = m_e c^2 / e B_0$. We can then rewrite the expression above

$$\frac{\beta_{sec} f_0 \sigma_{\gamma T} e^2 B_0}{4\pi \left( m_e c^2 \right)^2} \frac{\eta_{\text{max}}}{\eta_{\text{rad}}} \frac{\sigma_0^2}{\gamma_{\text{rad}}},$$

or, assuming $\eta \gg 1$,

$$\eta \approx (\beta_{sec} f_0)^{1/4(\gamma - 5)} \left( \frac{\eta_{\text{max}}}{\eta_{\text{rad}}} \frac{\sigma_0^2}{\gamma_{\text{rad}} \rho_0^5} \right).$$

(17)

We will compare this estimate with our simulations in section Section 4.2 where we describe our results.

---

In $\gamma$-ray pulsars, the power-law index of photons is close to $\Gamma \approx 1$–2 (Abdo et al. 2013). To estimate the multiplicity near the light cylinder, we can use the values of $\gamma_{\text{rad}}$ and $\gamma_{\text{rad}}$ defined in Equation (5) and take $n_0 = n_0 \Omega_{\text{pc}}$, where $\kappa \approx 10^4$ is the multiplicity of the primary cascade near the polar cap, and $n_{\text{pc}} \approx \Omega B_0 / 2\pi c e$. We will also assume that $s_1 = \rho_0 \approx 0.1 R_{\text{lc}}$.

We then find, for $\Gamma = 2$, that

$$\eta \approx 2 \times 10^4 \left( \frac{B_{\text{lc}}}{10^5 \text{ G}} \right)^{\frac{3}{2}} \left( \frac{P}{100 \text{ ms}} \right)^{2} \left( \frac{\rho_0}{0.1 R_{\text{lc}}} \right)^{\frac{1}{3}}$$

(18)

In particular, for the Crab ($B_0 \sim 10^6 \text{ G}$, $P = 33 \text{ ms}$), we find $\eta \approx 10^5$–$10^6$ for $\Gamma = 2$. Thus we expect pair loading to significantly affect reconnection near the Y-point.

---

3. Simulation Setup

We set up a 2D relativistic particle-in-cell simulation of a reconnecting current sheet using the code TRISTAN-MP (Spitkovsky 2005). The current sheet is initially in Harris equilibrium: cold (Maxwellian) upstream plasma with no bulk motion and a current sheet with hot plasma and bulk current (electrons and positrons having bulk velocities in opposite direction) to balance the magnetic field. The sheet is perturbed by either the artificial cooling of the central region or by adding a temporary magnetic loop near the center (see, e.g., Werner et al. 2018). In either case, the evolution does not depend on the way we trigger reconnection, and the later steady-state behavior is completely determined by our initial parameters.

Reconnection rapidly develops into the nonlinear stage where plasmoids are formed, advecting magnetic field loops and particles out of the box. While in one direction the absorbing boundary conditions allow plasma and fields to flow out (left and right boundaries on Figure 2), in the other direction the boundaries are being constantly extended while injecting seed primary plasma at rest in the far upstream (for more details, see Sironi & Spitkovsky 2014). This approach eliminates reflections from the boundaries. In the third unmodeled dimension, the boundary conditions are periodic.

The box size, $L$, is chosen so that $L / \sigma \rho_0 \gtrsim 50$, where $\rho_0$ is the gyroradius of a low-energy particle in the upstream field, and $\sigma$ is either the initial upstream magnetization parameter, $\rho_0$, or, in the case of pair production, the effective magnetization, $\sigma_{\text{eff}}$, which is much lower due to the mass loading by secondary pairs. After the reconnection starts, we wait until the transient plasmoids are advected out of the box, and the steady state is reached, and then turn on the cooling and pair production. We then wait for a few light-crossing times of the box until a new steady state is reached.

A charged ultra-relativistic particle ($\gamma \gg 1$, $\beta \approx 1$) in electromagnetic field experiences the radiation drag force (see, e.g., Landau & Lifshitz 1975),

$$F = -\frac{2}{3} r_e^2 \gamma^2 \epsilon (E + \beta \times B)^2 - (\beta \cdot E)^2,$$

(19)

where $r_e$ is the classical radius of the electron and radiates synchrotron photons. In our simulations, we define the effective perpendicular magnetic field,

$$B_{\text{eff}}^2 = (E + \beta \times B)^2 - (\beta \cdot E)^2,$$

which we will further use to compute the photon energy and the cooling rate. When the synchrotron cooling is enabled, each particle in our simulation probabilistically radiates a photon at
the corresponding synchrotron frequency set by the pair threshold parameter, $\gamma_c$,
\[ \epsilon_{\text{sync}} = m_e c^2 \left( \frac{\gamma}{\gamma_c} \right)^2 \left( \frac{B_{\text{eff}}}{B_0} \right) \left( \frac{\sigma_0}{10^7} \right)^{1/2}. \] (20)

where $B_0$ is the upstream magnetic field, and the last factor takes into account the magnetic field normalization (i.e., $\epsilon_{\text{sync}} \propto \gamma^2 B_0$). The photon radiation probability is set in such a way that the overall cooling rate, or the energy lost by a particle in a timestep, is consistent with the drag force in formula (18) and is controlled by $\gamma_{\text{rad}}$:
\[ \frac{\Delta \epsilon}{\Delta t} \propto \left( \frac{\gamma}{\gamma_{\text{rad}}} \right)^2 \left( \frac{B_{\text{eff}}}{B_0} \right)^2. \] (21)

Our simulation tracks photons as regular chargeless and massless particles propagating along straight lines with speed $c$. We do not track photons with very low energies (typically lower than $0.1\% – 1\%$ of $m_e c^2$), since they do not significantly contribute to pair production (for details, see Appendix B); they are, however, accounted for in particle cooling.

In each cell, every pair of photons can pair produce with a certain probability. We compute these binary probabilities for each pair of photons in the same cell according to Breit–Wheeler cross section and probabilistically create electron–positron pairs in that cell with momenta consistent with the differential cross section of the process. This algorithm naturally conserves both momentum and energy. Since we loop through all pairs of photons in each cell, this automatically ensures that the mean free path of every photon is inversely proportional to the number density of photons.

Magnetic reconnection in real astrophysical environments is controlled by a combination of the inflowing plasma density and the background magnetic field. Corresponding synchrotron energy is coupled to these parameters through the Planck’s constant, $\hbar$, while pair production cross-sectional magnitude is set by the Thomson cross section, $\sigma_T$. Particle-in-cell simulations without radiation can be made dimensionless by normalizing simulation parameters to plasma length- and timescales. Radiation and pair production introduce two extra scales (set by $\hbar$ and two-photon interaction cross section). We thus have four dimensionless parameters in our simulations:

1. The cold upstream magnetization parameter, $\sigma_c = \sigma_0$, and the radiation-reaction limit, $\gamma_{\text{rad}}$, set the background magnetic field and the effective plasma density, determining the available magnetic energy budget per particle and the rate with which particle energy is being transferred to radiation.
2. The pair threshold parameter, $\gamma_c$, sets the scale of the Schwinger field, $B_0$, with respect to the background magnetic field through relation (4). Given the total energy deposited into radiation (which is set by $\sigma_0$ and $\gamma_{\text{rad}}$), this parameter determines how this energy is distributed between photons, defining the Lorentz factor of the particle that radiates an MeV photon in the upstream field, as defined in Equation (3).
3. The effective mean free path to pair production is set by the fiducial dimensionless parameter $p_0$. In particular, the probability for two photons to produce $e^- e^+$ pair in one timestep is
\[ p(\Delta t) = p_0 \frac{\sigma_{\gamma\gamma}}{\sigma_T}, \] (22)

where $\sigma_{\gamma\gamma}$ is the Breit–Wheeler cross section described in Section 2.3 that depends on momenta and energies of the two photons, and $\sigma_T$ is the Thomson cross section. We choose a particular value of $p_0$ to ensure the small optical thickness of the overall system, while still producing enough secondary plasma. In Appendix A, we discuss in more detail how varying this parameter affects the regime we are simulating.

In order to accurately sample the photon momentum space in our typical runs, we would require on average $10^7 – 10^8$ photons per cell. To make this problem computationally feasible, we introduce “weights” for each photon and a merging routine to combine them. We use the algorithm described by Vranic et al. (2015) that merges all photons in the same momentum bin (and the same cell) to produce two “heavy” photons, while conserving energy and momentum without introducing any unnecessary momentum spread. Our momentum bins are uniform in direction and logarithmic in energy. To avoid artificial effects of binning, such as clumping of momenta in a particular direction, we change the orientations and sizes of these bins with times.

The disadvantage of this photon merging process is that it artificially decreases the pair production efficiency, as photons merged into a single “heavy” photon can no longer pair produce with each other. This turns out to have a weak effect on the results, because all the merged photons have small angles between their momenta and small relative energies, and so they have a small interaction probability according to Figure 3. While photon merging is as expensive as pair production in terms of computational time, it is crucial to implement to reduce the memory usage. As a result, we can reduce the number of photons by a factor of 10–100, while keeping the overall energy and momentum conserved and not strongly affecting the pair production.

In addition, we make several compromises in order to reduce both the time and memory consumption. Synchrotron cooling makes plasmoids effectively compressible, and in the strong cooling regime, the centers of plasmoids may get very high overdensities where the local skin depth becomes unresolved:
\[ \frac{c/\omega_p}{c/\omega_{p_0}} = (\gamma)^{1/2} \left( \frac{n_0}{n} \right)^{1/2}. \] (23)

Here, $\langle \gamma \rangle$ is the mean Lorentz factor of particles, which is typically of the order of $\sigma_0$ in plasmoid centers, $n/n_0$ is the particle overdensity compared to the upstream, and $c/\omega_p$ and $c/\omega_{p_0}$ are the local and upstream skin depths. To resolve the local skin depth with the same number of cells as in the upstream, we need to prevent overdensities larger than $\sim \sigma_0$. To alleviate this issue, we turn off the cooling in the very centers of plasmoids, where the overdensity compared to the upstream is above a certain value (typically few $\sigma_0$). As a result, the

5. The regions of large density where the cooling is artificially turned off are very small and are located deep in the middle of the plasmoids. We set the overdensity threshold for turning off the cooling, so that this region is just a few skin depths in size. This limiter does not affect the overall dynamics of the plasmoid, since the majority of particles still lie well beyond the very central region.
plasma cools down within the plasmoid until it reaches a particular distance from the center below which the cooling is turned off. The hot central region supports the plasmoid against further contraction; this has no noticeable effect on plasmoid motion. Upstream pair production is also not strongly affected by this effect, since the photons emitted in the centers would not escape the plasmoid due to a high optical depth inside. If the cooling were not turned off in the center, radiated photons would pair produce inside the plasmoid, feeding its interior with additional plasma until the plasmoid center cooled down and stopped emitting pair producing photons.

We also allow photons to escape into upstream from within the dense regions of plasmoids before they pair produce. This results in the lack of secondary plasma in the plasmoid interiors, which, however, does not affect the overall physics, since most of this plasma would be carried away with the plasmoids, unable to escape upstream.

4. Results

In this section, we will discuss our main simulation results. We first compare how synchrotron cooling and pair production individually affect the overall dynamics of reconnection and the formation and evolution of plasmoids. We then turn to particle acceleration and the emerging particle and photon spectra, again considering the effects of cooling and pair production separately. In most of our simulations, we take the upstream magnetization to be $\sigma_0 \sim 10^3$--$10^4$, in order to reach the desired high secondary plasma multiplicities. Cooling parameters $\gamma_e$ and $\gamma_{\text{rad}}$ are typically a few times $10^2$--$10^3$, to ensure that the number of high-energy photons is large enough and the cooling is in the strong regime. The cross-sectional magnitude, $p_0 = 10^{-5}$, is chosen so that enough pairs are produced (multiplicity $\gg 1$), but at the same time the optical depth to pair production is small across the box for all photons ($\tau_{\gamma\gamma} < 1$; see details in Appendix A).

4.1. Upstream Inflow and Plasmoids in the Steady State

In Figure 5 we show a snapshot of the plasma density (panels (b), (d), (f)) and the plot of the density averaged along the current sheet (panels (a), (c), (e)) for three different cases. For all the runs, we use three cells per cold skin depth, $c/\omega_{pe}$; initial plasma has five particles per cell, and the box size is $L = 7500$ cells $\times 2500 c/\omega_{pe}$. Our results are unchanged for different values of skin depth (3 to 10 cells), and the number of particles per cell (2 to 10). As a fiducial case, in Figures 5(a), (b) we show relativistic reconnection ($\sigma_0 = 5000$) without either synchrotron cooling or pair production. In Figure 5(c), (d) we show the result with synchrotron cooling turned on ($\gamma_{\text{rad}} = 1000$, $\gamma_e = 50$), but without pair production, and finally Figures 5(e), (f) show the run with pair production. Also, in Figure 6 we show the same snapshots as in Figure 5, but plotting the mean particle Lorentz factor in each cell to indicate the temperature of the plasma. For ease of comparison, all the corresponding colorbar scales are the same.

In the fiducial run (Figures 5(a), (b), and 6(a)), dense plasmoids contain most of the high-energy plasma particles (with $\gamma \sim \sigma_0$; see yellow regions in Figure 6(a)), accelerated in...
x-points and mergers. This hot plasma provides the pressure support for plasmoids against contraction due to the Lorentz force, $j \times B$. Interiors of plasmoids typically have higher magnetic fields and densities compared to both the current sheet and the plasmoid peripheries. In the presence of cooling (Figures 5(c), (d), and 6(b)), the high-energy particles within the plasmoids will be efficiently cooled to energies $< \gamma_{\text{rad}}$. We see in Figure 6(b) that the interiors of plasmoids have smaller average $\gamma$-factors compared to Figure 6(a). This removal of pressure support makes plasmoids compressive: they are now slightly smaller in size and are more dense and concentrated toward their centers (see Figure 5(c)).

When pair production is enabled (Figures 5(e), (f) and 6(c)), photons radiated in the current sheet and plasmoids escape to the upstream and pair produce with each other, additionally loading the system with secondary plasma (see Figure 5(f): both upstream and plasmoids are significantly denser compared to Figure 5(b), (d)). These upstream pairs inherit the power-law distribution function from the parent photons and are hot, as opposed to the cold inflowing primary plasma injected at the boundaries. This hot \(^6\) upstream can be seen as higher average Lorentz-factor plasma in the upstream region in Figure 6(c).

Pair production also decreases the effective magnetization. To demonstrate this effect, in Figure 7 we plot the cold, $\sigma_c \equiv B^2/4\pi\rho e^2$, and hot, $\sigma_h = \sigma_c/(\gamma)$, magnetization parameters, as well as the multiplicity of the secondary plasma, averaged along the $x$-axis and plotted against the $y$-axis. Figure 7(a) is the fiducial run without pair production or cooling, while Figures 7(b), (c) are for the run with pair production.

In Figure 7(a) we see that the cold magnetization parameter is very close to the far upstream value, $\sigma_0$, shown with a black solid line. On the other hand, pair production suppresses this number (Figure 7(b)) by a factor of $\eta + 1$, where $\eta$ is the effective multiplicity, also computed in situ \(^7\) (see Figure 7(c)). Note also that the hot magnetization, $\sigma_h$ (red line), in the case with pair production, differs strongly from $\sigma_c$ (blue line) even in the upstream. This underscores the fact that the upstream plasma, which is dominated by secondary pairs, is hot.

Pair production also has a strong impact on the overall dynamics and evolution of plasmoids. Figure 8 shows a typical snapshot from one of our pair producing simulations with higher $\sigma_0$. In this figure, we show the plasma density (Figure 8(a)), the density of high-energy photons with $h\nu > 50$ MeV (Figure 8(b)), and the local multiplicity (Figure 8(c)). Without pair production, the plasmoids can grow only through the slow accretion of plasma from upstream and through plasmoid mergers. When pair production is enabled, plasmoids radiate high-energy photons (Figure 8(b)), some of which can pair produce with the low-energy photons near the plasmoid peripheries (see high multiplicity regions in Figure 8(c)). This additional mass loading with hot secondary plasma produces more radiation that pair produces further, and the plasmoid continues to expand as it is being advected out of the simulation box.

In the real reconnection, this plasmoid growth will cease once the emitted photons can no longer pair produce near plasmoid peripheries. This can happen either because the optical depth across the plasmoid is large and the photons never escape from it, or because the plasmoid cools down and the

\(^6\) Here the terms “cold” and “hot” refer to the mean Lorentz factor of particles ($(\gamma) \sim 1$—cold, $(\gamma) \gg 1$—hot), which we used as a proxy for the characteristic particle energy. Note, however, that the distribution function of particles is a power law instead of a Maxwellian, and the mean Lorentz factor, strictly speaking, does not correspond to the thermal temperature.

\(^7\) The local multiplicity here is defined as the density of secondary pairs produced via two-photon pair production divided by the density of primary pairs originally injected from the boundaries.
radiated photons have energies that are too low. In our simulations, we allow these high-energy photons to escape from the plasmoids before they pair produce.

In addition, the mergers constantly eject new high-energy photons from freshly accelerated particles. These photons can then pair produce outside the current sheet, providing even more secondary plasma to the plasmoids. Because of this, plasmoids are typically larger and slower for higher multiplicities. When the sizes of plasmoids become comparable to the simulation box size, they effectively slow down the reconnection rate and in some situations can nearly stop it. After plasmoids leave the simulation box, the reconnection

Figure 7. Cold magnetization parameter, $\sigma_c = B^2 / 4\pi \rho c^2$, and hot magnetization parameter, $\sigma_h = B^2 / 4\pi (\gamma) \rho c^2$, averaged along the current sheet and over time for the runs without (a) and with pair production (b). Panel (c) shows the average multiplicity (density of secondary pairs divided by the density of primary pairs). Shaded regions show the interior of plasmoids where the multiplicity is suppressed artificially. Two solid black lines show the level of the upstream magnetization $\sigma_c$, which, when divided by multiplicity, gives the effective magnetization (black dashed line). In contrast to the case without pair production (a), when secondary plasma is produced the magnetization is reduced by a factor of multiplicity (b). Also, since the newly born pairs are hot, $\sigma_h$ is also reduced in the upstream.

Figure 8. Snapshot from a simulation of the reconnection with the cooling and pair production with $\sigma_0 = 10^3, \gamma_c = 50, \gamma_{rad} = 1000, p_0 = 10^{-5}$. The box extends further in the vertical direction; in this figure we focus on the large plasmoid. Plots show (a) the total plasma density normalized by the initial upstream density; (b) the density of photons with $h\nu > 50$ MeV; (c) the local plasma multiplicity, $\eta$, defined as the density of secondary plasma divided by the density of the injected plasma. Interiors of plasmoids are low in multiplicity since we allow photons to escape from them without having a chance to pair produce. Maximum density in the top plot (in white) indicates the region, where we turn off cooling to prevent plasmoids from getting too dense and making the local skin depth unresolved. When the pair production is enabled, the upstream is abundant with secondary plasma and also plasmoids are typically larger and slower, since they rapidly expand via pair production. In this snapshot, the massive plasmoid in the middle is undergoing mergers with smaller plasmoids, one of which (at $x = -300, y = -50$) has not yet been fully absorbed. Most of the photons are emitted within plasmoids close to their centers, where both the magnetic field and density are high. Lack of high-energy photons in the very middle of the large plasmoid is due to the fact that plasma in that region is cold. The full movie of this simulation is available online (direct link: https://youtu.be/VhwXzci_bY8).
continues with the regular rate at $\beta_{eq} \approx 0.1$--0.2. The movie of our simulation from Figure 8 that shows a large plasmoid and explosive photon ejections during plasmoid mergers is available online.\(^8\)

4.2. Particle Acceleration and the Emerging Radiation Spectra

We now focus on how cooling and pair production affect particle acceleration in reconnection, and how the resulting particle and photon spectra are formed. To distinguish the effects of cooling and pair production, we first analyze the process without pair production. We test how the cooling regime affects particle and radiated photon spectra (see, e.g., Kagan et al. 2016; Nalewajko & Yuan 2018).

The cooling regime is characterized by the ratio $\gamma_{rad}/\sigma_0$, which effectively sets the cooling time compared to the acceleration time $\sim (t_{cool}/t_{acc})^{1/2}$. If this ratio is $\gg 1$, the cooling is inefficient (i.e., the cooling time is much longer than the acceleration time and vice versa). Note, however, that this ratio is defined for the upstream magnetic field, so the actual cooling time of a particle will depend on the local magnetic field.

We initialize our simulations with the magnetization parameter $\sigma_0 = 200$ and cold plasma in the upstream. We fix $\gamma_e = 50$ and vary $\gamma_{rad}$ to study the different regimes. The results of our runs are shown in Figure 9, where we plot the particle and photon spectra (computed for the whole simulation domain) for the runs in different cooling regimes: from no cooling (yellow line) to strong cooling (dark blue line). The horizontal colorbar puts into correspondence the particle and photon spectra in particles; high-energy tails with $\nu F_\nu \propto \nu^{-1.2}$ are formed during transient mergers, when particles accelerated in secondary current sheets are captured by plasmoids and rapidly cooled.

followed by a steep decay at higher energies (close to a few times $\sigma \nu$; see Figure 9(a)).

The overall picture is then as follows: particles are accelerated in primary and secondary current sheets up to a few times $\sigma_0 c^2$. The magnetic field in these current sheets is weak, and the cooling time, $t_{cool}$, is much longer than the residence time in the $x$-points. This means that the cooling is inefficient close to the current sheets, and the particles remain hot until they are captured by the plasmoids, where they cool down to energies $< \gamma_{rad}$. Since the acceleration and cooling happen in different regions, we do not expect a different power-law slope or any pronounced power-law break in the particle distribution function close to $\gamma_{rad}$. The cutoff energy in particles is dictated by the acceleration in $x$-points, and is typically a few times $\sigma_0$. Note that there is no growth of this cutoff over time due to plasmoid compression, as found in the uncooled simulations of Petropoulou & Sironi (2018), because particles within the plasmoids are efficiently cooled to $\gamma_{rad}$ in our runs, unless the cooling is too weak $\gamma_{rad}/\sigma_0 \gg 1$.

The corresponding time-averaged photon spectra are shown in Figure 9(b). A standard result in the theory of synchrotron radiation is that particles constantly injected with a power-law energy distribution $f(\gamma) \propto \gamma^{-p}$ form a synchrotron spectrum described as $\nu F_\nu \propto \nu^{-(p-3)/2}$ (Rybicki & Lightman 1979). In our simulations, the plasma that resides within the plasmoids ($\gamma < \gamma_{rad}$) and forms a power-law spectrum with $p \approx 1$ radiates $\nu F_\nu \propto \nu$ synchrotron spectrum (see photon spectra before the peak in Figure 9(b)). The peaks in photon spectra correspond to particles with the energy $\gamma_{rad}$ radiating in magnetic fields of value close to the upstream field.

Photons with energies beyond the peak frequency are radiated by the particles with energies up to a few times $\sigma_0$. These particles enter the plasmoids after being accelerated in $x$-points and rapidly lose their energy, being exposed to a large perpendicular magnetic field, until they cool down to $\gamma \lesssim \gamma_{rad}$. As a result, the photon spectrum at high energies is highly fluctuating in time, since there is no steady population of high-energy particles ($\gamma > \gamma_{rad}$) in a large magnetic field. The majority of these high-energy photons, especially for the strong cooling regime ($\gamma_{rad}/\sigma_0 \ll 1$), are radiated during violent

---

\(^8\) Direct link: https://youtu.be/VhwXzci_bY8.
events such as plasmoid mergers. Averaged over time, these transients form an extended power-law tail (close to $\nu^{-1/2}$). We also present these results in the form of movies to better illustrate how the transients work both in strong and weak cooling regimes.\footnote{Direct links: https://youtu.be/QY_Bpjrp2Q and https://youtu.be/Mu_VY1ADhme.}

Further, we discuss the results of our runs with pair production. For all the runs described as follows, we choose the parameters to be $\sigma_0 = 10^3$ to $4 \times 10^4$, $\gamma_{\text{rad}} = 10^3$, $\gamma_c = 50$, and $p_0 = 10^{-5}$. These values are chosen to satisfy the relation $\gamma_c \ll \gamma_{\text{rad}} \ll \sigma_{\text{eff}}$ described in Section 2.2. We also want the synchrotron peak to be roughly at 0.1–1 GeV, which fixes $\gamma_c$ and $\gamma_{\text{rad}}$.

We first focus on a single value of $\sigma_0 = 5000$ to see how enabling pair production changes the shape of the particle and photon spectra. In Figure 10 we present the energy distribution of particles (Figure 10(a)) and photons (Figure 10(b)) for three runs: without cooling or pair production (yellow line), with cooling but without pair production (pink line), and with both cooling and pair production (blue line).

Cooling without pair production does not strongly affect the particle spectrum of $f(\gamma) \propto \gamma^{-1} - \gamma^{-3/2}$, in agreement with what we found earlier, only slightly decreasing the energy cutoff (see yellow and pink lines in Figure 10(a)). On the other hand, when pair production is on, the spectrum is no longer flat and there is no clear cutoff energy. Instead, particles form a wide power-law distribution, ranging from $\gamma^{-3}$ to $\gamma^{-4}$.

There are two effects causing this. First, since the layer is being mass loaded with secondary plasma, the effective magnetization parameter, $\sigma_{\text{eff}}$, decreases compared to the upstream magnetization, $\sigma_0$. This means that the reconnection has less magnetic energy per particle and the resulting spectrum shifts to lower energies. At the same time, the newly born secondary pairs (dashed blue line in Figure 10(a)) that have not yet been accelerated in the electric field at the x-point, form a steep power law with $f(\gamma) \propto \gamma^{-3} - \gamma^{-4}$ up to the highest energies. This means that, unlike with other cases where the current sheet was being fed by an initially cold plasma, in this case the upstream secondary plasma is already hot, due to a wide distribution in energies of parent photons that produced these pairs.

This behavior is also reflected in the photon spectrum (Figure 10(b)), where the peak is shifted due to the reduced magnetization. The peak in photons corresponds to $\gamma \approx \sigma$ in particles, where in the case of pair production, the value of $\sigma$ is reduced with respect to $\sigma_0$ by a factor of multiplicity. In this particular run, presented in Figure 10, the multiplicity is of the order of a few, and thus the effective magnetization is few times less than $\sigma_0$. The resulting peak frequency is proportional to the particle energy squared and is, therefore, smaller by roughly an order of magnitude.

Finally, in Figure 11 we show how the particle cutoff, box-averaged $\sigma_c$ (defined similar to Figure 7(b)) and spectral cutoff for photons depend on $\sigma_0$, i.e., the background magnetic field $B_0$ (since $\sigma_0 \propto B_0^2$ for fixed density). The average cold magnetization, $\langle \gamma_c \rangle$ (blue line in Figure 11(a)), is found by averaging $\gamma^2/4\pi\rho^2$ over a region around the current sheet where most of the pair production takes place. Different sizes of this region give different values, which we represent as errorbars. To determine the cutoffs we define a model-independent measure of how far our spectrum extends

$$\gamma_{\text{cutoff}} \sim \frac{\int d\gamma f(\gamma) \gamma^\alpha}{\int d\gamma f(\gamma) \gamma^{\alpha-1}},$$

and the same for photons (similar to what was done by Bai et al. 2015). This gives a rough estimate of where the spectral break (or the cutoff) is. Power $\alpha$ is empirically chosen to be between 2 and 3: varying $\alpha$ in that range gives different cutoff energies, which we present as errorbars (as a rough estimate of how wide and uncertain the cutoff is).

We compare our findings with the simple predictions without pair production feedback:

$$\gamma_{\text{cutoff}} \propto \sigma_0 \propto B_0^2, \quad E_{\text{cutoff}} \propto \gamma_{\text{cutoff}}^2 B_0 \propto B_0^5,$$
described in Section 2.4 with different values of the photon power-law index Γ.

First, note that both the cutoff energy and the magnetization are reduced compared to simple predictions without pair production feedback. This means that not only is the maximum energy of particles lower with pair production, but there is an effective upstream magnetization, σ_eff, that is decreased from the initial value σ_0 by a factor of multiplicity of secondary plasma.

From the runs with different values of σ_0, we find that the particle cutoff, γ_cutoff, grows roughly as B_0^{0.2–0.5} with the background magnetic field, and the photon spectral cutoff, E_cutoff, grows as B_0^{2–1.8}. These two scalings are consistent with each other, since E_cutoff ∝ γ_cutoff B_0. We can compare these results with simple predictions described by Equation (15). In our simulations, the distribution function of high-energy photons has a power-law index η ≈ 4–4.5 (corresponding to spectral index ν F_ν ∝ ν^{-1} – ν^{-2}). To zeroth order, scale lengths s_1 and s_2 from (15) can be taken to be equal to the size of the simulation box L. In these simulations, we have L/σ_0 ≈ 70(s_0/10^3)^{-1/2}, since the box has a fixed number of cells, but the gyroradii scales with the upstream magnetization. With s_1 = s_2 = L and η ≈ 1, we get roughly η ∝ σ_0, meaning that the effective magnetization scales weakly with σ_0: α = σ_0/(1 + η) ≈ const and E_cutoff ∝ B_0. Taking f_0 ≈ 0.1–0.01, β_{sec} ≈ 0.1, γ_c = 50, γ_red = 1000, and Γ = 3–4, we find that the steady-state multiplicity for σ_0 = 10^4 is η ≈ 2–10, while for σ_0 = 4 × 10^9 it is η ≈ 10–50, which roughly agrees with what we see. However, our simplified model does not account for time variability, we underestimate the multiplicity by a factor of a few, which results in a slightly higher effective magnetization (compared to (σ_0)).

To interpret these results in terms of observations, one should note that in these simulations we only varied the background magnetic field, while keeping the upstream plasma density constant. However, in reality, the inflowing plasma density from the inner magnetosphere to the Y-point depends also on the magnetic field and period of the pulsar, as the overall plasma density is normalized by Goldreich–Julian density n_{GJ} = Ω · B/2π e. This will further make the dependence of cutoff energy on the magnetic field at the light cylinder even weaker.

Another important observation in γ-ray pulsars is the dependence of the luminosity in γ-rays, L_γ, on the pulsar spin-down rate, ˙E. For most of the γ-ray pulsars (with the exception of millisecond pulsars) this dependence is sublinear, with a rough L_γ ∝ √˙E fit (Abdo et al. 2013). We can evaluate that dependence from our simulations. As L_γ, we take the energy deposited into the high-energy photons (>MeV) per unit time. On the other hand, we have the following two relations:

\[ ˙E ∝ B_{LC}^2 R_{LC}^2, \quad \sigma_{LC}^{(0)} ∝ B_{LC}^2 n_{GJ} ∝ B_{LC} R_{LC}, \]

where we assume that the spin-down energy is carried away in the form of the Poynting flux throughout the light cylinder. Here σ_{LC}^{(0)} is the primary magnetization without the feedback from pair production. We thus find that our σ_{LC} ≤ B_{LC} R_{LC}, or ˙E ∝ σ_{LC}^{0.5}, since the spin-down power, ˙E ∝ B_{LC}^2 R_{LC}^2, depends only on magnetization at the light cylinder.

Since the photon production is variable in time, we average L_γ over a large number of steps and present the time variability as errorbars. The results are shown in Figure 12, where we also overplot the observed L_γ ∝ √˙E trend, and the naïvely expected L_γ ∝ ˙E trend, which would be applicable if no pair formation were present. As seen in the plot, the observed dependence can indeed be understood if the pair production regulates the effective magnetization and thus the photon production in the current sheet.

5. Discussion

In this paper, we discussed the results of two-dimensional particle-in-cell simulations of radiative relativistic reconnection with pair production. We included both synchrotron cooling and two-photon pair production self-consistently by tracking all the radiated photons as separate particles and colliding them with each other. We then separately studied the effects of both cooling and pair production on particle acceleration and the emission signatures of reconnection. Our main findings are summarized as follows.
5.1. Synchrotron Cooling

1. Particles with energies $\gamma > \gamma_{\text{rad}}$ exist near the peripheries of plasmoids or close to the primary or secondary current layers, where cooling is inefficient. Bulk of the particles within the plasmoids have energies $< \gamma_{\text{rad}}$.

While in the case of non-radiative reconnection large plasmoids contain the bulk of the high-energy particles (with energies up to a few times $\sigma_c m_e c^2$), when synchrotron cooling is enabled these particles can no longer maintain their energies within the plasmoids due to the strong magnetic field. Thus the particles in plasmoids are cooled to energies $\gamma < \gamma_{\text{rad}}$ while the rest of the high-energy plasma, $\gamma > \gamma_{\text{rad}}$ exists either around the primary and secondary current sheets or in the vicinities of plasmoids, where the magnetic field is weak, and the cooling is inefficient.

2. Cooling removes the pressure support for plasmoids against contraction, and plasmoids become effectively compressive with typically smaller sizes and larger overdensities in the centers.

3. Weak cooling, $\gamma_{\text{rad}}/\sigma_c \gg 1$, preserves the hard power-law in particle energy distribution function $f(\gamma) \propto \gamma^{-1}$; in strong cooling regime, $\gamma_{\text{rad}}/\sigma_c \ll 1$, and the slope steepens toward $f(\gamma) \propto \gamma^{-\gamma_{\text{rad}}/\sigma_c}$.

Since the acceleration and cooling of the particles take place in different locations ($x$-points and plasmoids), there is no cooling break near $\gamma_{\text{rad}}$ and the power-law slope of the particle spectrum is generally unaffected.

4. The high-energy cutoff in particle distribution is only slightly shifted toward the lower energies (still being a few times $\sigma_c$). Because of that, the corresponding cutoff in photon spectrum is only marginally affected by cooling.

This maximum energy is roughly unaffected, because the $x$-points are still able to accelerate particles effectively up to a few times $\sigma_c m_e c^2$, as the cooling is inefficient in current sheets. However, once particles are captured by the plasmoids, where the magnetic field is high and the cooling time is short, they rapidly lose their energies. Because of that, we do not expect to observe any growth in particle cutoff energy with time for $\gamma_{\text{rad}} < \sigma_c$, as was predicted by Petropoulou & Sironi (2018) in the uncooled case.

5. For weak cooling, the peak in photon spectrum is set by the cutoff in particle spectrum (few times $\sigma_c$). For strong cooling, the peak in photons corresponds to $\gamma_{\text{rad}}$ in particle energy. Photons form $\nu F_\nu \propto \nu^{1/2}$ spectrum at low energies with a wide power-law tail at higher energies, close to $\nu F_\nu \propto \nu^{-1/2}$, up to a cutoff.

Photon spectrum beyond the peak is nonstationary with strong time variability, especially for stronger cooling regimes. Over time, these fluctuations add up to form a power-law tail. The time variability is primarily caused by plasmoid mergers, where particles are violently accelerated up to a few times $\sigma_c$ in secondary current layers and cool down by radiating high-energy photons when captured in merging plasmoids.

5.2. Two-photon Pair Production

Synchrotron photons, tracked in our simulations as regular massless and chargeless particles, can pair produce in the upstream and feed the current layer with secondary plasma. This process decreases the effective magnetization, suppressing the acceleration, and thus the radiation and further pair production.

1. Pair production drives the system to a self-regulated steady state, where the initial upstream magnetization, $\sigma_c$, is reduced by a factor of the resulting secondary plasma multiplicity.

Simple analytical model for this steady state predicts the following relation for the multiplicity of secondary plasma near the light cylinder in $\gamma$-ray pulsars (see Section 2.4),

$$\eta_{\text{LC}} \approx 2 \times 10^4 \left(\frac{B_{\text{LC}}}{10^3 G}\right) \left(\frac{P}{100 \text{ ms}}\right)^2 \left(\frac{R_{\text{LC}}}{32 L_{\text{LC}}}\right)^{1/3} \left(\frac{\beta_{\text{LC}}^2}{0.1 R_{\text{LC}}}\right),$$

where $B_{\text{LC}}$ and $P$ are the magnetic field at the light cylinder and the period of the pulsar, and $s_1$ and $s_2$ are the sizes of the regions where most of the radiation and pair production take place. For the Crab pulsar, this formula predicts $\eta_{\text{LC}} \sim 10^{-10}$.

2. Pairs produced in the upstream form an extended power-law slope, which they inherit from their parent photons. This makes the inflowing secondary plasma hot.

This effect causes the particle energy distribution to depart from the standard $f(\gamma) \propto \gamma^{-1}$ spectrum to form a wide power-law tail with indexes changing from $\gamma^{-2}$ at low energies to $\gamma^{-4}$ at higher energies.

3. Particles in the plasmoids radiate high-energy photons that can pair produce in the peripheries of these plasmoids. This process feeds plasmoids with newly born secondary plasma and causes the plasmoids to rapidly inflate. These “monster” plasmoids are typically larger and move slower than in the case of no pair production. They can capture a significant fraction of the simulation box, temporarily decreasing the reconnection rate.

4. In most of the runs with the radiation and pair production, $\sim 30\%$–$40\%$ of the total magnetic field energy in the box is deposited into particles and radiation equally (see details in the Appendix B). Resistive MHD (Kalapotharakos et al. 2012) and PIC (Philippov & Spitkovsky 2014)
simulations of the global magnetosphere predict that around 10% of the total Poynting flux in pulsars is dissipated near the light cylinder. Combined with our finding of the efficiency of relativistic reconnection for generating radiation, this means that a few percent of the spin-down energy is radiated as synchrotron radiation from the outer magnetosphere.

5. By running simulations of reconnection with different magnetizations, we find that \( \gamma_{\text{cutoff}} \propto B_0^{0.2–0.5} \), and the corresponding photon cutoff scales as \( E_{\text{cutoff}} \propto B_0^{0.2–1.8} \) with the background magnetic field, significantly weaker than without pair formation.

We did not vary the density of the inflowing primary plasma, which in the case of pulsars should scale with the corresponding Goldreich–Julian density near the light cylinder (thus with the background magnetic field near the light cylinder). This scaling would make the expected dependence on the magnetic field even weaker.

### 5.3. Observational Implications

In our simulations, we demonstrated that the effects of two-photon pair production are crucial to consider even in the optically thin regime, when most of the high-energy photons leave unaffected by pair production. We have shown that this effect leads to the weak dependence of synchrotron spectrum cutoff in pulsars on the magnetic field strength near the light cylinder. In particular, observations with \textit{Fermi Observatory} find \( E_{\text{cutoff}} \propto B_L^{1/2} - B_L^{1/2} \) (see Figure 1). This cutoff energy is set by the maximum energy of accelerated particles, \( \gamma_{\text{cutoff}} \), and the background magnetic field near the light cylinder (i.e., \( E_{\text{cutoff}} \propto \gamma_{\text{cutoff}} B_L \)). The particle energy cutoff is determined by the effective magnetization, \( \gamma_{\text{cutoff}} \sim \gamma_{\text{LC}} \propto \sigma_{\text{LC}} / \eta_{\text{LC}} \times E_{\text{cutoff}}^{1/2} / \eta_{\text{LC}} \) (with \( E \) being the spin-down power, proportional to the Poynting flux), which is smaller by the factor of multiplicity of the secondary plasma produced near the light cylinder. Then the photon cutoff energy can be written as \( E_{\text{cutoff}} \propto \dot{E} B_{\text{LC}} / \eta_{\text{LC}} \).

From our simulations, we find that \( \eta_{\text{LC}} \propto \sigma_0 \propto E_{\text{cutoff}}^{1/2} \) (see the last paragraph in Section 4.2), which roughly results in the dependence \( E_{\text{cutoff}} \propto B_{\text{LC}} \) and supports our previous assumption that the dependence on period is only included in the \( B_{\text{LC}} \).

For a more detailed application to \( \gamma \)-ray pulsars, this effect needs to be studied more closely using the global magnetospheric simulations (Philippov & Spitkovsky 2018).

In Figure 13 we show our estimations for the secondary plasma multiplicity in the current sheet, \( \eta_{\text{LC}} \), computed using Equation (27) from Section 2.4. Constant \( \eta_{\text{LC}} \) regions are plotted on a \( P-P \) diagram for known \( \gamma \)-ray pulsars, uncertainty of these regions are due to are due to the variation of the assumed photon index (within \( \Gamma \sim 1.5–2.5 \)). As one can see, the majority of the observed \( \gamma \)-ray pulsars should be very efficient in producing secondary pairs, \( \eta_{\text{LC}} \gg 1 \). Note, however, that here we assume the efficiency of polar pair production to be roughly \( \kappa \sim 10^4 \) for all pulsars, which might not be true (especially for the millisecond pulsars). Pulsars below \( \eta_{\text{LC}} \sim 1 \) line (X-ray pulsars) will not have enough high-energy radiation to substantially pair load the current sheet, and will thus have a much stronger dependency of the photon cutoff on the light cylinder magnetic field.

Our model also suggests that pair production in the outer magnetosphere may efficiently increase the density of the plasma escaping to the pulsar wind nebula. Observed injection rate of \( X \)- and \( \gamma \)-ray emitting particles to the PWN suggests multiplicities \( \sim 10^4 \) with respect to the average Goldreich–Julian density. This number is consistent with the upper limit provided by pair creation models from primary cascade near the polar cap (Timokhin & Harding 2019). However, observations of radio emission from low-energy plasma population implies a much higher limit on the ultimate multiplicity at the level of \( 10^5–10^6 \) for several different nebulae (Slane et al. 2010; Bucciantini et al. 2011; Arons 2012). In this paper, we argue that on top of the primary cascade near the polar cap, two-photon pair production in the outer magnetosphere can further enhance the density of the outflowing plasma. This can account to the anomalously rich low-energy plasma population in the PWN observed in radio.

It is important to emphasize that in the present paper, we studied the optically thin regime to both Thomson scattering and pair production, with only synchrotron radiation enabled, and with pair production driven by the interactions of these synchrotron photons. While this regime is applicable to pulsars, the process of two-photon pair production in reconnecting regions is ubiquitous and might be important in a wide range of astrophysical environments, in regimes where other QED mechanisms might also be important. We list some examples as follows:

1. \textit{Black hole accretion disk coronae} are thought to sustain reconnecting current layers with enough \( \sim \text{MeV} \) photons to trigger the production of secondary pairs. This effectively increases the Thomson optical depth of the layer to unity (Guilbert et al. 1983; Svensson 1987; Haardt & Maraschi 1993). In this optically thick environment, both the synchrotron and IC cooling as
well as the $e^-e^+$ annihilation are important to consider (Beloborodov 2017).

2. **Blazar jet flares** with durations of several hours to days have been interpreted as powered by large and slow plasmoids in the reconnection layer, where two-photon pair production of IC photons may play a crucial role (Ghisellini 2012; Petropoulou et al. 2016).

3. **Gamma-ray flares in SGRs** are also thought to be powered by relativistic reconnection with a near-critical magnetic field and with ongoing pair production driven primarily by $\gamma + B$ process (see, e.g., Thompson & Duncan 2001; Lyutikov 2006, studied in particle-in-cell by Schoeffler et al. 2019).

The approach introduced in this paper suggests a novel framework that could help incorporate additional pair production effects in particle-in-cell simulations in a self-consistent way. We plan to continue improving our algorithms and investigating these unexplored regimes in future work.

We thank Dmitry Uzdensky for initial discussions on implementation of pair production in PIC codes, Lorenzo Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments. This work was supported by NASA grant NNX15AM30G, NASA, through Einstein Postdoctoral Fellowship grant PF7-180165 awarded to AP by the Einstein Postdoctoral Fellowship grant PF7-180165 awarded to Sironi for fruitful conversations, and anonymous reviewer for constructive and insightful comments.

Appendix A
Details of the Algorithm

Since this is the first implementation of the self-consistent pair production in a particle-in-cell code, in this Appendix we present the details about the algorithm we used in our simulations.

We track two particle species: charged and massive plasma particles and massless photons. At each timestep, a plasma particle can radiate a photon (step (a) in Figure 14, left) with a corresponding synchrotron energy given by formula (20), and the overall cooling rate is set by relation (21). The photons are then resorted in memory according to their spatial location.

Since we intend to study the optically thin regime to pair production, $\tau_{\gamma\gamma} \ll 1$, and at the same time we have a sufficiently high multiplicity of secondary pairs, in our simulations the typical number of photons greatly exceeds the number of particles. This can very quickly exhaust the memory capabilities. To avoid this, we use a downsampling (merging) algorithm for the photons similar to one described by Vranic et al. (2015).

In each simulation cell, we define three-dimensional photon momentum bins and sort photons according to their momenta as seen in Figure 14, right. The bins are logarithmic in photon energies and uniform in 3D directions. We also randomly “rotate” the bins to minimize any downsampling artifacts. All the photons in the same momentum bin are then merged into two photons with higher effective weights (step (b) in Figure 14, left), conserving total energy and momentum. Note also that since the downsampling is done for the lowest energy photons (which are the majority) and for those who have small relative momenta angles, downsampling does not strongly affect the pair production efficiency, since those photons have a negligible probability to pair produce.

Two-photon pair production (step (c) in Figure 14, left) is another expensive step that we implement in our simulation. At each cell, we loop through all the non-repetitive pairs of photons and compute their binary probabilities $p_{ij}$ to pair produce, given their energies, momenta, and the cross-sectional formula.

Since the weights of those photons can be greater than one, these probabilities can also exceed unity (i.e., if $p_{ij} = 4.2$ on average from these photons, $i$ and $j$ we will create $4.2 e^-e^+$ pairs): four pairs with a probability 1 and one more pair with a probability 0.2 (reducing the photon weights each time). This approach is designed to mimic as if these interactions were between independent photons not merged into a two “heavy” ones.

The probability magnitudes are normalized to a fiducial parameter, $p_0$, which is chosen to ensure the low optical depth to pair production. Overall the optical depth for a photon can be...
production of our algorithm as a function of the total number of photons per cell along the path, $p_0$ is our fiducial parameter, and the prefactor $f_0$ accounts for the cross section for different energies and momenta orientation (see Figure 3) and is typically $0.1$–$0.01$. In our simulations, the size of the system is typically a few times $10^3$ cells, and the effective number of photon producing photons along the path can vary $10^2$–$10^3$ (less than the total number of photons per cell). This gives us a rough estimate that

$$\tau_{\gamma\gamma} \sim \frac{p_0}{10^{-3}}.$$  \hfill (29)

The difference between optically thick and thin regimes is demonstrated in Figure 15. The evolution of a single photon generation spectra are different in these two cases ($p_0 = 10^{-3}$ and $p_0 = 10^{-5}$). In optically thick regime (Figure 15, right), most of the high-energy photons interact with lower energy ones and pair produce in less than a single light-crossing time, resulting in a lower cutoff energy, whereas in optically thin regime (Figure 15, left), the spectrum nearly uniformly drops down over all energies due to pair production in a few light-crossing times.

Finally, in Table 1 we present the time and memory consumption of our algorithm as a function of the total number of photons, $N_{\text{ph}}$, and the average number of photons per simulation cell, $n_{\text{ph}}$. Pair production is the most expensive procedure, since it is $\sim \mathcal{O}(n_{\text{ph}})^2 N_{\text{cells}}) \sim \mathcal{O}(n_{\text{ph}} N_{\text{ph}})$.

Merging is efficient as far as the average number of photons per cell is $n_{\text{ph}} \gg N_{\text{bins}}$, where the number of momentum bins we typically use is $N_{\text{bins}} = 8^3 = 512$. In our typical run, we have $10^4$–$10^5$ photons per cell, and thus this downsampling significantly decreases the cost by reducing the number of tracked photons typically by a factor of $10$–$100$.

In most of our runs this is still expensive, and we do this procedure once every several steps, instead of doing it every step. One, however, should keep in mind that this interval cannot be longer than the typical mean free path of the photons to pair production (which in our case is a fraction of the box size), and also the interval should be short enough for the merging to prevent the memory exhaustion.

### Table 1

| Computational Cost | Memory Usage |
|--------------------|--------------|
| photon sorting     | $\mathcal{O}(N_{\text{ph}})$ | $\mathcal{O}(N_{\text{ph}})$ |
| photon merging     | $\mathcal{O}(N_{\text{ph}})$ | $\mathcal{O}(N_{\text{ph}})$ |
| pair production    | $\mathcal{O}(n_{\text{ph}} N_{\text{ph}})$ | $\mathcal{O}(N_{\text{ph}})$ |

### Appendix B

#### Radiation and Pair Production Statistics

We also present several diagnostic plots to justify our assumptions made earlier. Figure 16 (left) shows the two-dimensional histogram of the number of produced synchrotron photons plotted against the plasma particle energy and effective magnetic field that a particle experienced when radiating. Contour lines show the corresponding synchrotron energies. One can see that most of the photons are produced in a narrow range of magnetic field values from $0.1B_0$ to $B_0$, and the range gets even smaller for the higher energy particles, which are interesting in terms of pair production. Also it is clear that most of the photons are very low energy, which, however, do not strongly contribute to pair production. Thus it is important to correctly set the minimum tracking energy to make sure to capture enough pair production, but at the same time not to overwhelm the memory.

Figure 16 (right) shows the statistics of pair production from the same run, scatter plotted against the energies of two photons that produced the pairs. Each point is the pair production event, the color of each point represents the relative angle, $\phi$, between photon momenta. As one could have anticipated, the closer the energy product $\varepsilon_1 \varepsilon_2$ to $2m_e c^2$, the closer the relative angle to $180^\circ$, and vice versa: two high-energy photons can interact if their relative angle is small.

As one can also see from the one-dimensional histograms (Figure 16, right), the majority of pair production is for the photon energies $\varepsilon > 10^{-2} m_e c^2$, and thus the photon tracking energy limit (which in this case is $10^{-3} m_e c^2$) is justified. Two extended scatter “wings” to the right and up are due to the fact that some very high-energy photons do not have a low-energy partner to interact (not tracked), and are left to interact with the higher energy ones. These tails, while being a numerical
artifact, however, do not contribute much to pair production. We have carried convergence tests with lowering the energy limit with similar results: very low-energy photons do not have a significant contribution to pair production.

In Figure 17 the distribution of total energy in the box between different components is shown (normalized by the initial magnetic field energy, $U_B$). After the reconnection is triggered, we let the initial plasma escape through the boundaries perpendicular to the current sheet, which are being opened at around 1–2 light-crossing times. After that, new plasma (and thus magnetic flux) is injected at the boundaries, carrying additional energy, which is why we see that first spike in the plot. Most of the energy is carried by the magnetic field, which in the process of regular reconnection is being transferred to primary generation of particles up to 2–3 box light-crossing times. At that point, the synchrotron cooling and pair production are turned on and the reconnection relaxes to a new steady state.

At late times, the energy is mostly contained in photons and secondary particles created in pair production events. The large "waves" lasting a few box light-crossing times at late times are due to the large plasmoid, that constantly form, accumulate secondary plasma from the environment, and are then advected out from the box.

**ORCID iDs**

Alexander Philippov @ https://orcid.org/0000-0001-7801-0362

**References**

Abdo, A. A., Ajello, M., Allafort, A., et al. 2013, *ApJS*, 208, 17
Arons, J. 1983, in Positron-Electron Pairs in Astrophysics, Electron positron pairs in radio pulsars (Melville, NY: AIP), 163
Arons, J. 1996, *A&AS*, 120, 49
Arons, J. 2012, *SSRv*, 173, 341
Bai, X.-N., Caprioli, D., Sironi, L., & Spitkovsky, A. 2015, *ApJ*, 809, 55
Bai, X.-N., & Spitkovsky, A. 2010, *ApJ*, 715, 1282
Beloborodov, A. M. 2017, *ApJ*, 850, 141
Breit, G., & Wheeler, J. A. 1934, *PhRv*, 46, 1087
Bucciantini, N., Arons, J., & Amato, E. 2011, *MNRAS*, 410, 381
Cerutti, B., Philippov, A. A., & Spitkovsky, A. 2016, *MNRAS*, 457, 2401
Contopoulos, I., & Kalapotharakos, C. 2010, MNRAS, 404, 767
Coroniti, F. V. 1990, ApJ, 349, 538
Daugherty, J. K., & Harding, A. K. 1982, ApJ, 252, 337
Ghisellini, G. 2012, MNRAS, 424, L26
Giannios, D., Uzdensky, D. A., & Begelman, M. C. 2009, MNRAS, 395, L29
Guilbert, P. W., Fabian, A. C., & Rees, M. J. 1983, MNRAS, 205, 593
Guo, F., Liu, Y.-H., Daughton, W., & Li, H. 2015, ApJ, 806, 167
Guo, F., Li, X., Li, H., et al. 2016, ApJL, 818, L9
Haardt, F., & Maraschi, L. 1993, ApJ, 413, 507
Harding, A. K., & Kalapotharakos, C. 2015, ApJ, 811, 63
Kagan, D., Nakar, E., & Piran, T. 2016, ApJ, 833, 155
Kalapotharakos, C., Kazanas, D., Harding, A., & Contopoulos, I. 2012, ApJ, 749, 2
Landau, L. D., & Lifshitz, E. M. 1975, The Classical Theory of Fields (Oxford: Pergamon)
Loureiro, N. F., Schekochihin, A. A., & Cowley, S. C. 2007, PhPl, 14, 100703
Lyubarskii, Y. E. 1996, A&A, 311, 172
Lyubarsky, Y., & Kirk, J. G. 2001, ApJ, 547, 437
Lyubarsky, Y. E. 1995, Physics of Pulsars (Amsterdam: Harwood Academic)
Lyutikov, M. 2006, MNRAS, 367, 1594
Medin, Z., & Lai, D. 2010, MNRAS, 406, 1379
Nalewajko, K., & Yuan, Y. 2018, JPhPh, 84, 755840301
Petri, J. 2012, MNRAS, 424, 2023
Petropoulou, M., Giannios, D., & Sironi, L. 2016, MNRAS, 462, 3325
Petropoulou, M., & Sironi, L. 2018, MNRAS, 481, 5687
Philippov, A. A., & Spitkovsky, A. 2014, ApJL, 785, L33
Philippov, A. A., & Spitkovsky, A. 2018, ApJ, 855, 94
Rybicki, G. B., & Lightman, A. P. 1979, Radiative Processes in Astrophysics (New York: Wiley)
Schoeffler, K. M., Grismayer, T., Uzdensky, D., Fonseca, R. A., & Silva, L. O. 2019, ApJ, 870, 49
Sironi, L., Giannios, D., & Petropoulou, M. 2016, MNRAS, 462, 48
Sironi, L., & Spitkovsky, A. 2014, ApJ, 783, L21
Slane, P., Castro, D., Funk, S., et al. 2010, ApJ, 720, 266
Spitkovsky, A. 2005, in AIP Conf. Proc. 801, Astrophysical Sources of High Energy Particles and Radiation (Melville, NY: AIP), 345
Svensson, R. 1987, MNRAS, 227, 403
Tajima, T., & Shibata, K. 1997, Plasma Astrophysics (Reading, MA: Addison-Wesley)
Takata, J., Wang, Y., & Cheng, K. S. 2010, ApJ, 715, 1318
Thompson, C. 1994, MNRAS, 270, 480
Thompson, C., & Duncan, R. C. 2001, ApJ, 561, 980
Timokhin, A. N. 2010, MNRAS, 408, 2092
Timokhin, A. N., & Arons, J. 2013, MNRAS, 429, 20
Timokhin, A. N., & Harding, A. K. 2019, ApJ, 871, 12
Uzdensky, D. A., & Spitkovsky, A. 2014, ApJ, 780, 3
Vranic, M., Grismayer, T., Martins, J. L., Fonseca, R. A., & Silva, L. O. 2015, CoPhC, 191, 65
Werner, G. R., Philippov, A. A., & Uzdensky, D. A. 2019, MNRAS, 482, L60
Werner, G. R., Uzdensky, D. A., Begelman, M. C., Cerutti, B., & Nalewajko, K. 2018, MNRAS, 473, 4840
Werner, G. R., Uzdensky, D. A., Cerutti, B., Nalewajko, K., & Begelman, M. C. 2016, ApJ, 816, L8
Zenitani, S., & Hoshino, M. 2001, ApJL, 562, L63