Properties of bow-shock sources at the Galactic center

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ABSTRACT

Context. There exists an enigmatic population of massive stars around the Galactic center (GC) that were formed some Myr ago. A fraction of these stars has been found to orbit the supermassive black hole, Sgr A*, in a projected clockwise disk-like structure, which suggests that they were formed in a formerly existing dense disk around Sgr A*.

Aims. We focus on a subgroup of objects, the extended, near-infrared (NIR) bright sources IRS 1W, IRS 5, IRS 10W, and IRS 21, that have been suggested to be young, massive stars that form bow shocks through their interaction with the interstellar medium (ISM). Their nature has impeded accurate determinations of their orbital parameters. We aim at establishing their nature and kinematics to test whether they form part of the clockwise disk.

Methods. We performed NIR multiband imaging using NACO/VLT using direct adaptive optics (AO) and AO-assisted sparse aperture masking (SAM). We introduce a new method for self-calibration of the SAM point spread function in dense stellar fields. The emission mechanism, morphology, and kinematics of the targets were examined via 3D models, combined with existing models of the gas flow in the central parsec.

Results. We confirm previous findings that IRS 21, IRS 1W, and IRS 5 are bow-shocks created by the interaction between mass-losing stars and the interstellar gas. The nature of IRS 10W remains unclear. Our modeling shows that the bow-shock emission is caused by thermal emission, while the scattering of stellar light does not play a significant role. IRS 1W shows a morphology that is consistent with a bow shock produced by an anisotropic stellar wind or by locally inhomogeneous ISM density. Our best-fit models provide estimates of the local proper motion of the ISM in the Northern Arm that agree with previously published models that were based on radio interferometry and NIR spectroscopy. Assuming that all of the sources are gravitationally tied to Sagittarius A*, their orbital planes were obtained via a Monte Carlo simulation.

Conclusions. Our sources appear to be Wolf-Rayet stars associated to the last starburst at the GC. Our orbital analysis suggests that they are not part of any of the previously suggested coherent stellar structures, in particular the clockwise disk. We thus add more evidence to recent findings that a large proportion of the massive stars show apparently random orbital orientations, suggesting either that not all of them were formed in the clockwise disk, or that their orbits were randomized rapidly after formation in the disk.

Key words. massive stars – bow shocks – Galactic center – sparse aperture masking

1. Introduction

Sagittarius A West, the so-called mini-spiral, is a prominent feature of the interstellar medium (ISM) in the inner ~2 pc of the Milky Way (Ekers et al. 1983; Lo & Claussen 1983). It is made up of three streamers of ionized gas, termed the Northern, Western, and Eastern arms. Near- and mid-infrared observations of the mini-spiral show that the ionized gas is mixed with warm and hot dust that is in part arranged in complex structures like: extended filaments, bow-shocks and compact, barely resolved knots (Clénet et al. 2004b; Viebahn et al. 2006; Mužić et al. 2007). Studies of the radial velocities and proper motions of the gas in the mini-spiral have shown that their dynamics can generally be described by three bundles of quasi-Keplerian orbits in the combined potential of the central stellar cluster of the Milky Way plus a supermassive black hole (e.g., Vollmer & Duschl 2000; Paumard et al. 2004; Zhao et al. 2009).

It is generally thought that the gas in the mini-spiral is ionized by the radiation of more than one hundred massive, young stars that are located mainly within 0.5 pc of the supermassive black hole, Sagittarius A*, and that were formed in a star formation event about 2-6 Myr ago (Paumard et al. 2006; Bartko et al. 2010; Lu et al. 2013). Some of these young stars appear to orbit the black hole in a disk-like structure that rotates in a clockwise direction (referred to as clockwise system, CWS, in the following). This observation, along with the finding that the young stars are concentrated toward the black hole, gave rise to the currently favored hypothesis for their formation in situ in a formerly existing gas disk around Sagittarius A* (Levin & Beloborodov 2003; Paumard et al. 2006; Lu et al. 2009; Bartko et al. 2009).

Considerable open questions in this picture remain, however, in particular, concerning the nature of the young stars that are not part of the CWS (see, e.g., discussion in Genzel et al. 2010): is the second postulated system of a counterclockwise streamer or disk (CCWS) real? Is the CWS strongly warped? Can the current kinematical configuration of the young, massive stars be reached when one assumes that all of them are on the CWS? It is therefore of great interest to obtain as much information as possible about the orbital parameters of all young, massive stars.

Very many bow-shocks show evidence of interactions between stellar winds from the young massive stars and the ISM in the mini-spiral (Clénet et al. 2004a; Tanner et al. 2005; Geballe et al. 2006; Mužić et al. 2007; Buchholz et al. 2011). Some of these bow shocks are among the brightest near- to mid-infrared sources in the central parsec of the Galactic center (GC) and
have been known for decades \cite{Rieke1973, Becklin1975} before their nature was finally revealed through radiative transfer modeling and, in particular, high angular resolution imaging \cite{Tanner2002, Tanner2005}.

\cite{Tanner2005} analyzed high angular resolution near-infrared (NIR) observations of the sources IRS 1W, 5, 10W, and 21 and modeled their bow shocks. From the large measured stand-off distances of the bow shocks’ apices the authors concluded that the central sources must be Wolf-Rayet stars and thus were created in the above-mentioned star formation event. Because of the highly embedded nature of the sources, no spectroscopic confirmation of this classification could be obtained so far, with the exception of a tentative identification of IRS 1W as a Be star by \cite{Paumard2006}. The lack of suitable spectra means that the line-of-sight velocities of the bow-shock stars are unknown and cannot be used to estimate their orbital parameters.

Nevertheless, bow-shock (BS) sources are of great interest because they allow us, in principle, to infer all six of their phase space parameters, and thus one more (the line-of-sight distance) than in the case of other young stars. Their 2D positions and proper motions can be inferred from imaging. Their line-of-sight (LOS) velocities and distances can be inferred from their interaction with the mini-spiral and from the resulting shape of the bow shocks in combination with models of the gas flow in the mini-spiral \cite[e.g.,][]{Vollmer2000, Paumard2004, Zhao2009}. In this way, \cite{Tanner2005} were able to show that the kinematic properties of IRS 1W and 10W, as determined from their measurements, are consistent with the hypothesis that these stars belong to the CWS. However, they did not have the necessary proper motion measurements to perform this kind of analysis on IRS 5. For IRS 21, \cite{Tanner2005} were unable to resolve its bow-shock and concluded that it was seen face-on \cite[see also][]{Tanner2002, Buchholz2011}, however, were recently able to resolve the bow-shock structure of IRS 21 through deconvolution of high-quality adaptive optics data and could thus discard the face-on hypothesis.

Here we continue the investigation of the bow-shock sources IRS 1W, 5, 21, and 10W by \cite{Tanner2005}. We use our own multiwavelength AO assisted imaging as well as AO-assisted sparse aperture masking (SAM) \cite[see, e.g.,][]{Tuthill2006a} to investigate the structure of the sources, which we then fit with fully 3D models. The results from the modeling are then combined with new, more accurate proper motion measurements and with models of the mini-spiral flow to investigate the kinematics of the bow-shock stars.

Section 3 describes the acquisition and reduction of the data. The calibration process and image reconstruction of our SAM observations is described in particular detail because we describe a novel way of self-calibrating SAM data in a dense stellar field. This procedure can be of general interest for SAM observations of targets in dense stellar fields. Section 4 describes the results of the proper motion measurements. Section 5 describes the mathematical model used in determining the shape and emission of the bow shocks and the corresponding fitting procedure. Section 6 describes the local kinematics of the Northern Arm at the position of the bow shocks and the procedure of determining the probability density function of the source orbital planes. Finally, in Sect. 7 we discuss our results and present our conclusions.

| Date       | Filter | N° | DIT [s] | Camera |
|------------|--------|----|--------|--------|
| 03 May 2002 | K      | 60 | 20     | S27    |
| 10 May 2003 | K      | 2280 | 0.5 | S27    |
| 12 Jun 2004 | IB,2.06 | 96 | 30     | S27    |
| 13 May 2005 | K      | 6180 | 0.5 | S27    |
| 29 Apr 2006 | K      | 896  | 2     | S27    |
| 28 May 2008 | K      | 104  | 10    | S27    |
| 31 Mar 2009 | K      | 1920 | 1     | S27    |
| 28 Sep 2010 | K      | 2016 | 1.0    | S27    |
| 17 May 2011 | K      | 143  | 2.0    | S27    |
| 03 May 2009 | K      | 109  | 3     | S13    |
| 21 Jul 2009 | H      | 138  | 10    | S13    |
| 03 Jun 2010 | L      | 20   | 5     | L27    |
| 03 Jun 2010 | NB,3.74 | 6   | 20    | L27    |
| 04 Jun 2010 | L      | 30   | 5     | L27    |

\textsuperscript{a} Number of exposures.
\textsuperscript{b} Detector integration time. The total integration time of each observation amounts to N\times DIT.
\textsuperscript{c} The pixel scale of the NACO S27 camera is 0.027′/pixel, that of S13 is 0.013′/pixel.
\textsuperscript{d} Used for proper motion measurements.
\textsuperscript{e} Imaging observations used to investigate the structure of the bow shocks.
\textsuperscript{f} SAM observations used to investigate the structure of the bow shocks.

2. Observations and data reduction

2.1. AO imaging

We used AO-assisted imaging observations of the central parsec of the GC with VLT/NACO to measure the proper motions of the bow-shock sources and to infer their structure. Table 1 summarizes the observations. The bright supergiant IRS 7, located about 5.5″ north of Sgr A*, was used to close the loop of the AO. IRS 7 is a variable source \cite{Ott1999}. The most recently published values for its flux are $K_s = 7.69 \pm 0.06$ in April 2006 and $K_s = 6.96 \pm 0.04$ in March 2009 \cite{Schodel2012}. All imaging data were sky subtracted, flat fielded, corrected for bad pixels, and then combined via a shift-and-add algorithm into final mosaics, as described, for instance, in \cite{Schodel2009}. The saturated cores of bright stars were repaired in all images from epochs 2002 to 2008. The images from 2009 to 2011 did not need to be repaired since saturation was not a problem because of the short exposure times used for these observations. The data from 2010 and 2011 were taken with NACO’s cube mode, which registers each individual exposure \cite{Girard2010}. To improve the image quality of the latter data we applied a lucky imaging method and selected the 30% of the frames with the highest Strehl ratios.

To remove the seeing halos in the AO images, we extracted point spread functions (PSFs) from the $H$- and $K_s$-band images that were obtained with the S13 camera of NACO and deconvolved the images with the Lucy-Richardson algorithm \cite{Lucy1974}. The deconvolved images were restored with a Gaussian beam of 2 pixels FWHM to create the final images to be used in our analysis.

2.2. Observations with sparse aperture masking

Our SAM observations of the GC central parsec were performed in the nights of 3/4 and 4/5 June 2010 with VLT/NACO.
used the L.7 camera (0.027′/pixel) and chose two combinations of filters and mask: the $L'$ broad-band filter ($\lambda_{\text{central}} = 3.80 \mu m$, $\Delta \lambda = 0.62 \mu m$) was combined with the $BB_{\text{holes}}$ mask and the $NB_{3.74}$ narrow-band filter ($\lambda_{\text{central}} = 3.74 \mu m$, $\Delta \lambda = 0.02 \mu m$) with the $9_{\text{holes}}$ mask. The latter combination reduces bandwidth smearing, while the first combination leads to higher sensitivity. The observations were recorded using pupil tracking.

The wide field of view (FOV) ($27'' \times 27''$) of the L.7 camera allowed us to observe all targets simultaneously. All SAM data were pre-processed according to standard imaging data reduction, that is, sky subtraction, flat-fielding, and bad-pixel correction.

Depending on the observational data sets, the sky was obtained by calculating either (i) the median of separate sky observations obtained on a dark cloud about 400'' north and 700'' west of Sagittarius A*, or (ii) via the median of the appropriately clipped values at each pixel from the dithered images on-target when no dedicated sky observations close in time were available. We note that sky subtraction did not result in a completely flat background as expected. Instead, patterns remained in the images, probably because of the rapid and variable atmospheric conditions. However, these patterns varied on scales of $\sim 2''$, that is, on scales larger than the size of the SAM PSFs. Their impact on the calibration of the SAM observations was therefore considered not significant. A reduced individual image frame ($L'$, $BB_{\text{holes}}$) is shown in Fig. 1.

The so-called cube mode was used to save each single-detector integration time (DIT) frame. The advantage of this mode is that it allows selecting the best frames. In our case, frame selection was necessary because atmospheric conditions (and the AO correction) were affected by highly variable seeing and the passage of clouds. About 80% of the frames were de-selected (using a simple flux criterion on the star IRS 7). The final set of data consists of a group of 13 cubes composed of 20–30 exposures with 5 s and 20 s DIT each for $L'$ and $NB_{3.74}$ filters, respectively. Finally, the selected frames for each of the individual targets were stored into separate cubes of $128 \times 128$ pixels.

The standard observing technique for SAM requires closely interwoven observations between calibrator and target. The calibrator must be a nearby point-like source (within $\sim 1'' - 2''$). We obtained observations of the calibrator sources HD 161718 and HD 162907. A dither pattern was used in which the source was located at the center of the four quadrants of the detector so that the sky could be extracted by a simple median superposition of the dithered target observations.

### 2.3. Extraction and calibration of the interferometric observables from the SAM data

For the subsequent processing of the SAM data we used an IDL pipeline developed at Sydney University (priv. comm., M. Ireland). This code constructs a matched filter for the given instrumental setup (pixel scale, observing wavelength, filter, aperture mask) and uses it to measure the squared visibilities, $V^2$, for all interferometric baselines as well as the bispectra, which are the ensemble of the visibility products for all non-redundant baseline triangles. The arguments of these bispectra are the closure phases (CPs). The CPs provide information of the point-symmetry of the source and are free of telescope-dependent phase errors induced by atmosphere and telescope vibrations. Finally, to eliminate the baseline-dependent errors, the calibrated $V^2$ were obtained by the ratio of the raw $V^2$ of the target and calibrator, while the calibrated CPs were obtained by subtracting the calibrator CPs from the CPs of the target.

We note that the $u - v$ coverage ($u - v$ refers to the coordinates in the interferometric plane, i.e., the coverage of the Fourier transform of the image) of the targets in our observation was not limited by the properties of the interferometric masks used, but was increased through Earth rotation synthesis by combining observations of the targets at different parallactic angles.

To accurately calibrate the SAM observations, it is generally recommended to frequently switch between the target and the calibrator while leaving all AO settings unchanged. But this was not possible for our observations because of the highly variable conditions (seeing, clouds) that made changes to the AO setting necessary, delayed calibrator observations, and led to unstable correction. We thus lacked sufficient, adequate calibrator observations.

One of the possible solutions to overcome this problem was using the IRS 7 star as calibrator because it is contained in all our SAM frames. This source was already tested and used by Tuthill et al. (2006b) as a calibrator for SAM observations. However, they performed their observations at shorter wavelengths than we did. IRS 7 is known to be surrounded by extended emission at MIR wavelengths (Viehmann et al. 2006), which may already show some contribution at the long NIR wavelengths used here. In addition, the images of IRS 7 may have been affected by local systematic variations of the background and do not properly reflect the variance of PSF and background for the entire FOV of our observations.

To overcome these problems we developed a technique that we called the synthetic calibrator. This method takes advantage of the many bright sources in a crowded FOV as is the case for the GC. The procedure is very similar to the iterative extraction of an empirical PSF from a crowded field that is implemented in PSF fitting algorithms such as StarFinder (Diolaiti et al. 2000). We used StarFinder to (i) select the brightest stars in the SAM...
Fig. 2. Calibrated squared visibilities and closure phases for the SAM observations of IRS 1W. Orange circles: calibration with the synthetic calibrator technique. Blue circles: calibration with IRS 7 as calibrator. The CPs values are plotted over the spatial frequency of one of the three baselines used to compute each one of them.

This technique provides a reliable way to minimize the contribution of all the potential systematic errors related to each one of the individual sources. Even more, the synthetic calibrator is robust, under certain constraints, to the use of slightly extended sources as inputs (like IRS 3). These restrictions require that the in-going sources have no strong closure phase information (i.e. the source is not asymmetric) and that their emission is dominated by the point-like source. We can observe, at first glance, in Fig. 1 that the four sources used to build the synthetic calibrator fulfill the requested constraints and have a significantly crispier PSF than our science targets.

We used the few valid calibrator observations to verify this technique by comparing the calibrated $V^2$ and CP values that were obtained with the synthetic calibrator and with a real calibrator. No systematic differences were found. We also compared the resulting calibrated $V^2$ and CP obtained with the synthetic calibrator and with IRS 7 as calibrator. Again, the values agreed within their uncertainties. This also confirms that IRS 7 is unresolved with the chosen SAM setup. Figure 2 shows a comparison of the calibrated $V^2$ and CPs using the synthetic calibrator technique and IRS 7 as calibrator for one of our sources. We decided to use the synthetic calibrator technique to calibrate the $V^2$ and CP of all our targets. Figure 2 illustrates the information that can be obtained from our SAM measurements: IRS 1W is completely resolved-out for baselines longer than 4 meters, which indicates that the source angular size is extended and larger than 120 milliarcsec; the closure phases differ significantly from zero, which excludes a point-symmetric structure for the source.

We note that the synthetic calibrator technique can only be used when several sufficiently bright sources are present within the FOV and when the PSF is not expected to vary significantly over the FOV. It may be ideal for observations of stars in dense clusters, where it can both improve the calibration of SAM data and boost the efficiency of SAM observations because it does not require any change of the instrument setup and avoids overheads caused by calibrator observations.

2.4. SAM image reconstruction

Image reconstruction from the interferometric data was performed with the BSMEM package (see, e.g., Buscher D. F. 2013, Lawson et al. 2004). This code uses a maximum-entropy algorithm. Table 2 lists the number of iterations and the reduced $\chi^2$ values at the end of the deconvolution process for all sources.

Table 2. Iterations and reduced $\chi^2$ for BSMEM image reconstruction

| Source    | Iterations | $\chi^2$ |
|-----------|------------|----------|
| IRS 1W    | 15         | 1.10     |
| IRS 5     | 15         | 1.86     |
| IRS 10W   | 12         | 2.31     |
| IRS 21    | 20         | 1.82     |

The size of the beam used in the reconstruction procedure is $\theta=60$ mas, which corresponds to the nominal angular resolution reached by this technique for the filters we used. The pixel scale used for the reconstruction process was 13 mas/px.

3. Proper motions

To measure the proper motions of the stellar sources at the center of the bow shocks we used VLT/NACO $K_s$-band AO imaging data obtained between 2002 and 2011 (see Table 1). Schödel et al. (2009) obtained proper motion measurements of our sources using PSF fitting to measure their stellar positions. This method is not suited for extended sources like the bow shocks that we analyze here, however. Instead, we measured the stellar positions by centroiding the emission maxima of the central stars in circular apertures of with a radius of 4, 5, and 6 pixels. The positions and their uncertainties were taken as the mean of the three measurements and its corresponding uncertainty. Note that measuring stellar positions by aperture centroiding is significantly less susceptible to systematic errors caused by (moderate) saturation or nonlinearity than is PSF fitting. Moreover, since the bow shocks are extended targets, PSF
focusing on the central stars is very difficult and prone to systematic errors.

Astrometric alignment was achieved with the help of the known positions and proper motions of a sample of about 200 stars contained in all images. The astrometric reference stars were selected from the list published by Schödel et al. (2009). The stars had to be brighter than $K_s = 12$, with no companion within 0.3'' and the uncertainty of each component of the proper motions of the reference stars had to be smaller than $< 30 \text{ km s}^{-1}$. These criteria ensure accurate aperture measurements of their positions.

We transformed the stellar positions into the astrometric reference frame via a second-order polynomial fit (see Appendix A in Schödel et al. 2009). A Monte Carlo approach was used to estimate the uncertainty of this alignment procedure, with 1000 trials. For each trial the positions of the reference stars were varied randomly, with the offsets drawn from Gaussian distributions with standard deviations corresponding to the positional uncertainty of each star at each epoch.

After obtaining the stellar positions for each epoch, we fitted the data points by linear motions. The reduced $\chi^2$ was generally significantly larger than 1. There were some sources of uncertainty that were not specifically taken into account, such as errors introduced by camera distortion into the mosaics, the shape of the bow shocks, pixel saturation, or faint secondary stars within the aperture laid over the bow shocks. Hence, the uncertainties of the stellar positions may have been underestimated. This is no serious problem, however, because we can be certain that linear motions are accurate models to describe the proper motions. Therefore, the uncertainties of the linear fits were all rescaled to a reduced $\chi^2 = 1$. This procedure avoids underestimating the uncertainties (see Schödel et al., 2009, for a more elaborate discussion). The measured angular velocities were converted into km s$^{-1}$ by assuming a Galactic center distance of 8 kpc (e.g., Schödel et al. 2010). Plots of position vs. time along with the linear fits for the proper motions are shown in Appendix A.

Table 3 lists the proper motions of the bow-shock sources and of the stars IRS 16NW and IRS 33N as determined here and by Schödel et al. (2009). IRS 16NW and IRS 33N are two point-like sources that we used as a reference point to compare our method and Schödel et al. (2009). The measurements of IRS 16NW and IRS 33N and of the bow-shock sources all agree within their 1σ uncertainties, with the exception of IRS 1W. We believe that the discrepancy on the latter source is probably due to the PSF fitting technique used by Schödel et al. (2009), which is poorly suited to strongly resolved/extended sources like IRS 1W. Moreover, IRS 1W is one of the brightest sources in the field and is affected by saturation in many images. Aperture fitting is suited to both extended and (moderately) saturated sources. We therefore believe that the proper motions for the bow-shocks’ stellar sources that we have derived here may be more accurate than those published by Schödel et al. (2009). Tanner et al. (2005) measured the proper motions of IRS 21, IRS 1W, and IRS 10W, which are also listed in Table 3. Their measurements generally agree with ours within the quoted 1σ uncertainties, with the exception of the velocity along the right ascension of IRS 21. Note that the proper motions of Tanner et al. (2005) suffer from very large uncertainties, possibly because of the small FOV that they used for determining the proper motions and because they used images reconstructed from speckle observations that have a significantly lower signal-to-noise ratio than we used (AO imaging).

4. Modeling the bow shocks

4.1. Bow-shock images

In Fig. 3 we show a compilation of our images of the bow-shock sources IRS 1W, IRS 5, IRS 10W, and IRS 21. The bow shock is clearly resolved in almost all sources in at least one wavelength. IRS 21 and IRS 10W are more clearly resolved than in the work of Tanner et al. (2005), which can be attributed to technological progress. While Tanner et al. (2005) used low Strehl shift-and-add reconstructed speckle data, here we use high Strehl and high signal-to-noise AO images and images reconstructed from AO assisted sparse aperture masking, a technique that provides a precise calibration of the PSFs. Note that Buchholz et al. (2011) and Buchholz et al. (2013) presented a resolved image of the bow shock around IRS 21. Hence, this source is not seen face-on as hypothesized by Tanner et al. (2005) (see also Tanner et al. 2002).

The extended emission becomes stronger toward longer wavelengths, a consequence of the temperature of the dust in the bow shocks. Tanner et al. (2002) derived a dust temperature of ~1000 K for IRS 21. Viehwang et al. (2006) also showed that the temperatures of the bow-shock sources peak at around 4-10 µm, consistent with a dust temperature of a few hundred degrees. On the other hand, the central star is only detected at the shorter wavelengths (see Fig. 3).

4.2. Bow-shock shape

The shape of the bow shocks results from the interaction between the stellar wind and the surrounding ISM. Assuming a steady-state model, the shape of the bow shock results directly from the stand-off distance, $R_0$, where the ram pres-
In units of $R_0$

The 2D polar can be determined by the momentum of the shocking winds, (ii) that the shell is a thin layer of negligible width, and (iv) that the interacting winds are homogeneous and do not change with time. The cooling process is instantaneous, (iii) that the shell is a thin layer of negligible width, and (iv) that the interacting winds are homogeneous and do not change with time. The two polar angles $\phi$ and $\theta$ are shown (see Eqs. 2 and 3). The blue axis is centered on the position of the star and the scale is in multiples of $R_0$. The inset in the upper-right part of the diagram shows the change in bow shock inclination angle as seen from the observer.

The cells of the bow shock are defined by sampling $R_{3D}(\theta, \phi)$ with increments in $\theta$ and $\phi$ of 0.5° (see Fig. 4).

### 4.3. Bow-shock emission

#### 4.3.1. Polarization and emission mechanisms

[Buchholz et al. (2013)] described that the bow-shock sources, particularly IRS 21 and IRS 1W, exhibit strong polarization levels at NIR wavelengths. The polarization increases from shorter to longer wavelengths, highlighting the importance of the extended dust component. Polarization of the extended emission and of the embedded bow-shock sources in the Northern Arm (NA) reaches its maximum in the MIR (see [Glasse et al. 2003]). Buchholz et al. (2011) found that the polarization of the bow-shock sources IRS21 and IRS 1W agrees with the orientation of the magnetic field in the NA. These authors also suggested that the ordered magnetic field is responsible for the dust grain alignment in the bow-shock shells. The polarization measurements from NIR to MIR thus support the assumption that the emission in the bow shocks is produced by the dust IR thermal emission, which is reprocessed UV light from the central star.

#### 4.3.2. Bow-shock emission model

Although the previously mentioned findings suggest that the bow-shock emission is mainly produced by thermal emission, we also explored the role of scattered light in the bow-shock emission, particularly at shorter wavelengths. The procedure used to simulate the emission maps was similar to the one developed by [Muzic et al. (2010)]. The dust thermal emission, $L_{th}$, was assumed to have a blackbody source function attenuated by the corresponding optical depth, that is, $L_{th} \propto B(T_d) (1 - e^{-\tau_{abs}})$. The dust temperature distribution in the bow shock ($T_d$) is assumed to be created by heating the dust by the stellar photospheric UV photons from the central source. Therefore, under this condition, $T_d$ is computed via the [van Buren & McCray (1988)] solution,

$$T_d = 27 a_{\mu m}^{-1/6} L_{\nu}^{1/6} r_{pc}^{-1/3} K,$$

where $m_*$ is the mass-loss rate of the star, $v_*$ is the velocity of the stellar wind, $\rho_{ISM}$ is the density of the surrounding ISM, and $v_*$ is the relative velocity between the star and the ISM.

To obtain a steady-state solution for the bow-shock shell, [Wilkin (1996)] assumed (i) that the bow-shock shape is determined by the momentum of the shocking winds, (ii) that the cooling process is instantaneous, (iii) that the shell is a thin layer of negligible width, and (iv) that the interacting winds are homogeneous and do not change with time. The 2D polar canonical form of a bow shock, under the previous conditions, is then defined by

$$R(\theta) = R_0 \csc \theta \sqrt{3(1 - \theta \cot \theta)},$$

where $\theta$ is defined as the angle from the axis of symmetry to any point on the 2D-shell’s surface. To extend the previous relation from 2D to 3D, we let the locus of $R(\theta)$ rotate by angle $\phi$ as shown in Fig. 4, hence

$$R_{3D}(\theta, \phi) = \text{rot}(R(\theta), \phi), \quad 0° \leq \phi \leq 180°.$$

**Fig. 4.** 3D Diagram of the bow-shock shell created by our model. The diagram is sliced and the interior of the bow shock is visible. The two polar angles $\phi$ and $\theta$ are shown (see Eqs. 2 and 3). The blue axis is centered on the position of the star and the scale is in multiples of $R_0$. The inset in the upper-right part of the diagram shows the change in bow shock inclination angle as seen from the observer.

**Fig. 3.** Images of the bow-shock sources. Each line corresponds to a different source, while the three columns show the Lucy-Richardson and beam-restored images in the $H$- and $K_s$-bands, and the image reconstructed from the $L'$-band SAM observations.
where $a_{cm}$ is the grain size in microns, $L_{38}$ is the star UV luminosity in units of $10^{38} \, \text{erg/s}$ and $r_{0}$ is the distance to the dust from the star in parsecs. After calculating the contribution from each cell, the total $L_{tot}$ was normalized to one.

The scattering emission was computed using the normalized Henyey & Greenstein (1941) source function modified by the optical depth, $L_{sca} \propto r_{cm}P(\theta_{sca})e^{-\tau_{sca}}$, where $r_{cm}$ is the distance to the dust from the star in centimeters. The scattered light is described by

$$P(\theta_{sca}) = \frac{(1 - g^2)}{(1 + g^2 - 2g\cos(\theta_{sca}))}^{1/2}, \quad (5)$$

where $g$ is a dimensionless term that depends on the scattering angle $\theta_{sca}$, with $g = 0$ when the scattering is fully isotropic and $g < 1$ when the scattered light preserves the angle of incidence. After calculating the contribution from each cell, the total $L_{sca}$ was normalized to one. The previous treatment of the scattering emission does not take into account the polarization of light, only the deflection angle of the incident radiation in the dust. A more detailed model of the scattering emission is beyond the scope of this work.

The total bow-shock emission, $L_{tot}$, at every cell in the model was computed adding the previously normalized thermal and scattering emissions. $L_{tot} = L_{th} + L_{sca}$, where the coefficients $\epsilon_{th}$ and $\epsilon_{sca}$ are the relative efficiencies ($\epsilon_{th} + \epsilon_{sca} = 1$) of the thermal and scattering contribution. The optical depths, $\tau_{th}(\lambda)$ and $\tau_{sca}(\lambda)$, at every cell of the 3D bow-shock shell are calculated as

$$\tau_{th}(\lambda) = \int_{a_{th}}^{a_{0}} n_{th}(a)C_{th}(a, \lambda)da, \quad (6)$$

$$\tau_{sca}(\lambda) = \int_{a_{sca}}^{a_{0}} n_{sca}(a)C_{sca}(a, \lambda)da, \quad (7)$$

where $C_{th}(a, \lambda)$ and $C_{sca}(a, \lambda)$ are the dust thermal and scattering extinction coefficients. They are calculated as $C_{th}(a, \lambda) = \pi a^2(Q_{abs})$ and $C_{sca}(a, \lambda) = \pi a^2(Q_{sca})$. The values of the thermal and scattering efficiencies, $Q_{abs}$ and $Q_{sca}$, were obtained from the Draine database on the optical properties of interstellar dust grains.\footnote{http://www.astro.princeton.edu/d\slash\dust/dust.diel.html} For a standard mixture of 50% graphite and 50% silicate (see Mathis 1990, Draine & Lee 1984). The grain size distribution used, $n_{th}(a)$, follows an MRN (Mathis et al. 1977) power-law with the grain size $a$ ranging from $a_{\text{min}} = 0.005 \mu m$ to $a_{\text{max}} = 0.25 \mu m$.

4.4. Bow-shock fitting

We used the 3D steady-state model and the dust emission processes described in the two preceding sections to create models of the bow-shock shells and fit them to the images. The best-fitting models were found by a $\chi^2$-minimization as implemented in the IDL MPFIT package by C. Markwardt (Markwardt 2009).

Masks were applied to the bow-shock images to suppress features that are not related to the actual bow shocks. Each masked image was normalized to unity inside the applied mask. The same normalization was applied to the projected and masked models. A central point-source was included in the model (with free parameters for its position and flux). This point-like source concentrates most of the NIR-flux and dominates the model fitting at the shortest wavelengths. We note that the pixel uncertainties are hard (or impossible) to determine in Lucy-Richardson deconvolved images and in the BSMEM reconstructed images.

In addition, there are several sources of systematic uncertainties, such as faint point sources or ISM features that may be confused with the bow shocks. Therefore, both uniform and flux-weighting schemes were tested to determine the model with the lowest uncertainties that is least affected by the systematics previously discussed. Our tests show that a flux-weighting scheme produced better fits in $H$ and $K_s$ while a uniform weighting works better in $L'$. The final uncertainties of the best-fit parameters are obtained from their standard deviation of the fits to the statistically independent images from the three different filters. We also expect this procedure to reliably take care of possible contamination from stars and extended emission because the former are expected to be faint at $L'$ and the latter at $H$.

The stand-off distance $R_0$ (reported in Table 4), which is strongly degenerated with the inclination of the bow shock, was linked in our fitting code to the projected stand-off distance in the plane of the sky, $R_0 = R_0/cos(i - 90^\circ)$, where $i$ is the bow-shock inclination angle between the LOS and the bow-shock apex. When the bow-shock apex is pointing to the observer $i = 0^\circ$ and when the bow-shock shell is projected in the plane of the sky $i = 90^\circ$ (see inset in Fig. 4), $R_0$ was obtained from the mean of a Gaussian fit to the emission obtained by three radial cuts along the bow-shock structure. The central cut was made along the symmetry axis of the bow shock, the two additional cuts were at $-10^\circ$ and $+10^\circ$ from the position of the central cut. Figure 4 shows as an example the radial cuts, the fitted Gaussian, and the $R_0$ mean value obtained for IRS5 in the $H$-filter. A similar procedure was performed for the other sources. The rest of the parameters described in Table 4 were fitted directly to the image described at the beginning of this section.

4.5. Contribution from dust scattering to the bow-shock emission

To quantitatively approximate their relative importance, we investigated the effect of different relative thermal and scattering efficiencies on our models. Since IRS 5 appears to resemble the canonical steady-state bow-shock model most, we used the images of this source in $H$ and $K_s$ to perform this test. We fit different sets of models with fixed efficiencies for thermal and scattering emission at different wavelengths and considered cases of isotropic and anisotropic scattering. For each wavelength, model fitting was performed with increments of 10% in the scattering efficiency from 0 to 70% of the total emission observed. We tested the cases for $g=0$ in the scattering source function.
(isotropic scattering) and for \( g = 0.5 \) (partially anisotropic scattering).

The best-fit bow-shock model was found in each trial with the procedure described in Sect. 4.4. Residual images were obtained by subtracting the models from the original image. Figure 6 displays the sum of the squared pixel values of the residuals in the \( H \) filter and the lower one to the residuals in the \( K_s \) filter for isotropic scattering.

**Fig. 6.** Sum of the squared residuals of the best-fit models with increasing relative contribution of scattering emission. The upper panel corresponds to the residuals in the \( H \) filter and the lower one to the residuals in the \( K_s \) filter for isotropic scattering.

In the right panel shows the length of the bow-shock tail. It has a length of \( \sim 0.8'' \) or 6400 AU. The radial lines emanating from the apex of the bow shock of IRS 1W are artifacts of the high-pass filtering.

**Fig. 7.** Left: \( L' \)-band image of the surroundings of IRS 1W. Right: highpass-filtered version of the image. The white arrow in the right panel shows the length of the bow-shock tail. It has a length of \( \sim 0.8'' \), or 6400 AU. The radial lines emanating from the apex of the bow shock of IRS 1W are artifacts of the high-pass filtering.

(continued)

**Table 4.** Best-fit parameters of our bow-shock models for IRS 5 (spherically symmetric stellar wind)

| Parameter | \( H \) | \( K_s \) | \( L' \) | \( \sigma_{\text{rms}} \)
|-----------|---------|---------|--------|------------------|
| \( R_0 \) [AU] | 445.0 ± 34.9 | 517.0 ± 34.9 | 575.0 ± 34.9 | ±53.0 ± 10.0 |
| P.A. [deg] | 50.0 ± 1.2 | 46.9 ± 1.2 | 47.0 ± 1.2 | ±1.6 ± 0.3 |
| Inclination [deg] | 116.0 ± 1.2 | 139.9 ± 1.2 | 144.6 ± 1.2 | ±12.5 ± 2.0 |
| FWHM [px] | 2.0 ± 0.1 | 2.23 ± 0.1 | 4.6 ± 0.1 | - |
| Bow-shock flux [%] | 60.0 ± 1.2 | 90.0 ± 1.2 | 100.0 ± 1.2 | - |

\( a \) The standard deviation of the measurements obtained in the three filters.

\( b \) Position angle increasing E of N.

\( c \) Angle between the the bow-shock symmetry axis and the observer’s line of sight. 0° - the bow-shock apex is toward the observer, 90° - the bow-shock is projected on the plane of the sky.

\( d \) Full width at half maximum of the beam at different wavelengths in pixels. The FWHM reported for the \( L' \)-band is fixed and corresponds to the synthesized beam of the SAM observations.

\( e \) Percentage of the total emission that corresponds to the extended emission. The rest of the emission corresponds to the central source.

**4.6. Properties of the individual sources**

Here, we discuss the individual bow-shock sources in detail. Their morphologies can be examined in Fig. 5 while Fig. 10 shows the best-fit bow-shock models overplotted to the images.

**IRS 5:** This bright bow-shock displays similar morphologies in the \( H \) and \( K_s \) filters. The central star is clearly identified in \( H \) and \( K_s \). The projected bow-shock shape is axially symmetrical in the plane of the sky with the vector from the central star to the stagnation point. IRS 5 is the source in our sample that can best be described with the isotropic wind steady-state model. Table 4 describes the best-fit parameters for the different wavelengths. Here, and for the other bow-shock sources, we conservatively estimate the uncertainties of the best-fit parameters from their standard deviation that results from the fits to the images at the different wavelengths (i.e., we did not use the uncertainty of the mean). The small uncertainties support the model assumption of a bow shock in the steady-state phase. Our results suggest that the bow shock of IRS 5 is inclined at \( \sim 130° \).

From the interaction of IRS 5 with the NA and using the NA model of [Paumard et al. (2004)], we estimate a position of \( z = 3.81'' \pm 2.66'' \) along the line-of-sight (LOS), where \( z = 0 \) corresponds to the plane of the sky. Assuming that IRS 5 is gravitationally bound to Sgr A*, we calculate a 3 \( \sigma \) upper limit of \( \pm 336 \) km s\(^{-1} \) for its LOS velocity.

**IRS 1W:** as Fig. 3 shows, the target is resolved at the three wavelengths. It has a clear bow-shock structure in \( K_s \) and \( L' \), but also deviates from the analytical bow-shock model that we used here: first, a rounded shell appears around the central star that is open on its southern edge and is clearly visible at \( H \) and \( K_s \). It is not observed in \( L' \), however. Instead, the tails of the bow shock are better distinguished. The origin of this more rounded shell in the \( H \) and \( K_s \) images is unclear. Second, the shape near the apex is slightly asymmetrical in \( L' \), with the maximum of the emission shifted to the west of the apex. Possible causes are confusion with a star or some feature in the mini-spiral, or an asymmetrical outflow from IRS 1W. To investigate this point further, the left panel in Fig. 7 shows a close-up of the surroundings of IRS 1W from a NACO \( L' \)-band image. The right panel shows a highpass-filtered version of the same image. IRS 1W does not appear to be contaminated by a typical mini-spiral feature such...
Fig. 8. Model of a bow shock in an ISM with a quadratic density gradient. The $L'$ image of IRS 1W is represented in color and the best-fit gradient model is overplotted as contours. The colored vectors represent the velocity of the star ($V$; green arrow), the relative motion of the star through the ISM ($V_{rel}$; ISM; blue arrow) and the dust motion of the ISM obtained with our bow-shock model ($V_{ISM}$; red arrow).

as a thin filament, nor by any bright star (see also Fig. 3). We therefore do not find any obvious or easily testable explanation for the observed asymmetry, but note here that the mini-spiral is generally a complex region with many knots and features in the ISM that may be confused in projection and/or interact with the bow shock. Third, IRS 1W displays a long, tightly closed tail. The tail of IRS 1W is clearly visible in the highpass-filtered image and has a length of approximately 0.8″, or 6400 AU.

IRS 1W shows a remarkable interaction with the ISM of the NA. The proper motion of IRS 1W is $350 \pm 25$ km s$^{-1}$ at an angle $332 \pm 5^o$ E of N. Assuming a mass of $4.2 \pm 0.3 \times 10^6 M_\odot$ for Sgr A* (Gillessen et al. 2009; Yelda et al. 2011), the escape velocity at the projected distance, $R = 5.30 \pm 0.01$″, of IRS 1W is $419 \pm 15$ km s$^{-1}$. The LOS distance of IRS 1W can be estimated from its interaction with the Northern Arm of the mini-spiral. Using the model of Pauvard et al. (2004), we estimate a LOS distance of $z = 7.37 \pm 1.3^o$ for IRS 1W and obtain an escape velocity of $320 \pm 29$ km s$^{-1}$ at its 3D position. Although this is lower than its proper motion, both values overlap well within their 1σ uncertainties. Using the 3σ upper limit in the escape velocity and the 3σ lower limit on the proper motion, we can set a firm upper limit of $V_z = 300$ km s$^{-1}$ on the LOS velocity of IRS 1W (assuming that it is bound to Sgr A*, of course). This corresponds to a maximum inclination of its velocity vector of $137^o$, corresponding to $47^o$ out of the plane of the sky, moving away from the observer. Here, the ambiguity between motion toward or away from the observer is broken by our best-fit bow-shock model. From the model of Pauvard et al. (2004) we can calculate the properties of the gas flow. At the position of IRS 1W, the gas in the NA has a proper motion of $226 \pm 70$ km s$^{-1}$ at an angle $207 \pm 13^o$ E of N. The orientation of the tail-like feature agrees well with the relative proper motion between star and gas. The angle of the gas flow out of the plane of the sky is a mere $7^o$, with the gas moving toward the observer, which means that the NA flow is practically within the plane of the sky at the position of IRS 1W. We note that with a relative proper motion between star and gas on the order of $550$ km s$^{-1}$ the channel-like feature that is marked by the tail of IRS 1W may trace the motion of IRS 1W over the past ~50 years. With such short timescales at work, IRS 1W may be an ideal probe for the conditions of the ISM in the NA, for instance, for the homogeneity of the gas density.

Table 5 shows our best-fit bow-shock model for IRS 1W using our steady-state model. The second row of images in Fig. 10 corresponds to the steady-state isotropic wind-fitted models. As can be clearly seen, our model cannot fit the tail of IRS 1W well (specially in $L'$) because it is much narrower than what can be produced with this model. Possible explanations of this problem include (i) changes in the density of the ISM at the shocking points, (ii) variations in the mass-loss rate and wind velocity, (iii) anisotropic winds, or (iv) that because of the short interaction times the bow shock in IRS 1W has not yet reached the steady-state bow-shock solution (see Mohamed et al. 2012). The large scatter in the best-fit position angles in Table 5 also suggests that the isotropic wind model is not suitable to reproduce the observed morphology of IRS 1W.

To examine whether there are other models that provide a better fit to the IRS 1W morphology, we decided to perform a model fitting using the narrow solution of a steady-state bow-shock model described in Zhang & Zheng (1997). We assumed that the central source has a wind bound inside a cone with an opening angle of $40^o$ along the polar axis. Table 6 displays the fitted parameters and the third row of images in Figure 10 represents the best-fits for the narrow solution. A comparison between the isotropic wind model and the narrow solution (see Fig. 10) demonstrates that the latter fits the observed emission of IRS 1W better, with the main difference being in a smaller $R_0$ and different inclination. The narrow solution models have considerably lower residuals and result in best-fit parameters with very low scatter between the different observing wavelengths.

Another plausible explanation for the shape of IRS 1W can be changes in the density of the ISM. This condition is not rare in complex environments like the NA where filaments and clumps of gas/dust are observed. For example, Rauch et al. (2013) determined the geometry and emission of the asymmetric IRS 8 bow shock using a shell solution for a quadratic density gradient in the NA ISM. Figure 8 displays our best-fit solution to IRS 1W in $L'$ for an ISM density gradient. The density gradient function has the form $\rho = \rho_0 (1 + a_1 x + a_2 y)$, where $\rho_0$ is the mean density of the ISM and x and y the direction of the $p_0$ increment. In our model, the density increased from east to west and the values of the coefficients $a_1$ and $a_2$ were fixed to 2.0 and 5.0, respectively. This bow-shock gradient solution produced residuals on the order of those of the narrow solution. Similar values were obtained between the narrow and the gradient solution for the fitted parameters. The best-fit gradient solution produced a $R_0 = 533$ AU, and inclination of $i = 103^o$ and a PA=9°. Nevertheless, to perform a complete least-squares fitting to bow-shock solutions with free gradient coefficients and/or different gradient functions creates strong degeneracies among the fitted parameters. Hence, we did not investigate other gradient solutions and decided to use the narrow solution best-fit model for the following analysis. Although we cannot fully distinguish between the physical mechanisms that produce the observed shape of IRS 1W, our narrow and gradient models suggest that inhomogeneities in the stellar wind and/or ISM are important in shaping the structure of this particular bow shock.

IRS 10W: the extended emission around this source presents a particularly different morphology in $L'$, more so than in $H$ and $K_s$. The central star is detected in the $H$ and $K_s$ filters. Extended emission is observed at the position of the central source in $L'$. It is unclear whether this emission is related to the central star or not. The projected emission in $H$ and $K_s$ displays a symmetric
Table 5. Best-fit parameters of our bow-shock models for IRS 1W (spherically symmetric stellar wind)

| Parameter          | $H$   | $K_s$ | $L'$ | $\sigma_{\text{rms}}$ |
|--------------------|-------|-------|------|------------------------|
| $R_0$ [AU]         | 689.0 | 606.0 | 651.0| ±54.0                  |
| P.A. [deg]         | 3.0   | -13.0 | 27.0 | ±10.0                  |
| Inclination [deg]  | 130.0 | 121.0 | 127.0| ±4.0                   |
| FWHM [px]          | 2.0   | 3.24  | 4.6  |                        |
| Bow-shock flux [%] | 49.0  | 79.0  | 100.0|                        |

Table 6. Best-fit parameters of our bow-shock models for IRS 1W (narrow solution)

| Parameter          | $H$   | $K_s$ | $L'$ | $\sigma_{\text{rms}}$ |
|--------------------|-------|-------|------|------------------------|
| $R_0$ [AU]         | 520.0 | 523.0 | 523.0| ±1.2                   |
| P.A. [deg]         | 13.0  | 2.0   | 5.0  | ±5.0                   |
| Inclination [deg]  | 88.0  | 96.0  | 84.0 | ±5.0                   |
| FWHM [px]          | 2.0   | 3.42  | 4.6  |                        |
| Bow-shock flux [%] | 50.0  | 79.0  | 100.0|                        |

Fig. 9. Left: $L'$-band image of the surroundings of IRS 10W. The filamentary structure of the NA is appreciated as well as some additional close-by stars with extended emission. Right: the reconstructed SAM image of IRS 10W in $L'$ band. An asymmetric structure can be seen. Contours represents 10, 20, 30, 40, 50, 60, 70, 80, and 90% of the peak flux.

Because of the asymmetric shape of IRS 10W in $L'$, we decided to apply the model fitting only to the $H$ and $K_s$ images. Table 7 shows the best-fit parameters. The fourth row of images in Figure 10 displays the best-fit models in contours. Although the extended emission around IRS 10W can be interpreted as a bow shock, a more detailed analysis of the IRS 10W proper motion and of the NA motion (at the position of IRS 10W) does not support the idea of a bow shock produced by the relative motion of the star throughout the ISM.

IRS 10W has a proper motion of $217\pm14$ km/s with a PA of $355^\circ$ E of N (see Fig. 10 and Table 3). Paumard et al. (2004) reported a gas flow of $189\pm84$ km/s with a PA of $188^\circ$ E of N at the position of IRS 10W, while the values according to Zhao et al. (2009) are $229\pm49$ km/s with a PA of $191^\circ$. Therefore, the relative proper motion of IRS 10W with respect to the NA is $403\pm86$ km/s at a PA of $1^\circ$ E of N, or $441\pm37$ km/s at a PA of $3^\circ$ E of N, that is, at a PA perpendicular to the direction of the possible bow-shock symmetry axis (around $-90^\circ$). This suggests that the extended emission around IRS 10W is not produced by the bow-shock model described in Sect. 4.2, which implies that the relative motion and the bow-shock axis must be parallel. Alternative explanations for the observed extended emission are (i) a shock between the stellar wind with a dust knot or filament of the NA, (ii) a shock between the stellar winds of IRS 10W and a secondary source, or (iii) a chance superposition of a some NA feature with IRS 10W. These hypotheses are plausible since IRS 10W is located in a very mixed environment of the extended emission in the NA, some filaments can be observed superimposed along the source position and, additionally, some close-by stars have extended emission (see Fig. 9).

IRS 21: the bow-shock of this source can be clearly seen at all wavelengths and is similar to the deconvolved $K_s$-band image presented by Buchholz et al. (2011). IRS 21 is best resolved in H band, where the central star is also unambiguously detected. We can discard the hypothesis, made by Tanner et al. (2005), that IRS 21 is seen face-on, since these authors could not resolve its structure in their lower Strehl no-AO observations. In our $K_s$ and $L'$ images the central source is not detected and the bow-shock morphology is less clearly observed because of the lack of angular resolution. We therefore decided to apply the model fitting only to the $H$-band image. The steady-state model fits the morphology observed in the $H$-band very well. The proper motions of the star and of the NA environment are consistent with the relative motion of the bow shock obtained from our model. Table 8 lists the best-fit parameters.

Since we only performed the model fitting to the IRS 21 $H$-band image, the uncertainties in the fitted parameters were estimated in a different way than for the other bow shocks, for which we have at least two models in two different filters. For IRS 21, the uncertainties reported in Table 8 were estimated by testing three different starting values for the bow-shock inclination angle. We chose this approach because the inclusion angle strongly affects the determination of the bow-shock stand-off distance. In fact, it is degenerated for low- and high-inclinations and therefore, our code works best at intermediate values of inclination angles ($40^\circ \leq \alpha \leq 160^\circ$). Very low- or high-inclination angles result in bow-shock shapes that resemble spherical shells. Thereupon, our code cannot compute the stand-off distance since it strongly depends on the inclination angle (see Section 4.2.2). For IRS 21 we tested the code with initial conditions of $i = 50^\circ$, $90^\circ$, $145^\circ$. The fitted parameters are reported in Table 8 and their errors are the standard deviation of the three trials. Although the model did not always converge to the same solution, which can be largely explained by degeneracies between the model parameters, the best-fit parameters, resulting from the runs with significantly different starting values for the inclination, have overall similar best-fit parameters with a low scatter between them.
Fig. 10. Bow-shock fitting of IRS 1W, IRS 5, IRS 10W and IRS 21 in H, K_s and L' wavelengths. We represent in colors the real image and in contours the best model obtained. The colored vectors represent the velocity of the star ($V_s$; green arrow), the relative motion of the star through the ISM ($V_{s-ISM}$; blue arrow) and the dust motion of the ISM obtained with our bow-shock model ($V_{ISM}$; red arrow).

5. ISM velocity field and bow-shock orbital parameters

5.1. Northern Arm dust motion

Our best-fit bow-shock models provide estimates of the local motion of the ISM in the NA. Assuming that our objects are
Table 8. Best-fit parameters of our bow-shock models for IRS 21 (steady-state)

| Parameter       | $H_{\perp,50}$ | $H_{\perp,90}$ | $H_{\perp,145}$ | $\sigma_{\text{rms}}$ |
|-----------------|----------------|----------------|----------------|----------------------|
| $R_0$ [AU]      | 432.0          | 417.0          | 462.0          | ±22.0               |
| P.A. [deg]      | -8.5           | -4.0           | -6.3           | ±2.2                |
| Inclination [deg]| 106.0          | 95             | 116            | ±10.0               |
| FHWM [px]       | 2.14           | 2.11           | 2.05           | ±0.04               |
| Bow-shock flux [%]| 68.0           | 62.0           | 65.0           | ±3.0                |

Wolf-Rayet stars (Tanner et al. 2005) with a mass-loss rate on the order of $m_\infty \sim 1-2 \times 10^{-5} M_\odot/yr$ and stellar winds with velocities around $v_\infty \sim 1000 \text{ km s}^{-1}$, and that the density in the NA has a mean particle number $n_{HI} \sim 3 \times 10^3 \text{ cm}^{-3}$ (see Tanner et al. 2002; Rauch et al. 2013), we first calculated the relative velocity between star and ISM with Eq. 1. Subsequently, we determined the measured proper motion of the central star to calculate the proper motion of the ISM at the position of the bow-shocks. Figure 10 shows the projected motion of the ISM, $V_{\text{ISM}}$, relative to the motion of the bow shock, $V_\text{bow}$, according to our best-fit model (blue vector), and the proper motion, $V_c$, of the central source (green vector) for all our targets. All our ISM motion measurements (magnitude and position angle) agree to within 1-$\sigma$ with the models of Paumard et al. (2004) and/or Zhao et al. (2009) except for IRS 10W, which supports our hypothesis that IRS 10W does not represent a standard bow shock (see section 4.5). Table 8 summarizes the NA projected motions obtained in this work and the previously published models of gas and dust. These results corroborate the hypothesis of Wolf-Rayet stars as the central sources of the bow shocks. For comparison, if we compute the projected NA motions using O-stars, $(m_\infty \sim 10^{-7} M_\odot/yr; v_\infty \sim 2000 \text{ km s}^{-1};$ Prinja et al. 1990) as the central engines of the bow-shocks, the resulting NA motions are a factor of ~5-10 lower than the observationally inferred values. Hence, we discard the idea of O-stars as the central sources of the bright NA bow shocks.

5.2. Orbital motion of the bow-shock sources

The location of the sources that we studied within the NA and the determination of their geometry with the models used here provide valuable information to determine the probability density distribution (PDF) of their orbital parameters, $PDF(a, e, i, \Omega, \omega, P, T_0)$. We used the methodology described by Lu et al. (2009) and the same definitions for the orbital elements. This method consists of a Monte Carlo simulation of $10^5$ trials to convert the 3D positions and velocities of the sources into their six orbital parameters. The projected positions of the bow shocks are obtained from the astrometric measurements used to compute their proper motions (see Sect. 3). The distances of the bow shocks along the LOS and their respective uncertainties were obtained from the NA model of Paumard et al. (2004). The LOS velocities were constrained in two different ways. On the one hand, they were constrained by assuming that the sources are tied to the gravitational potential of SgrA* and have a 3D motion lower than their escape velocities. This method provides an upper limit for the magnitude of the LOS velocity but with an ambiguity in its sign. The PDFs of the orbital parameters were therefore constructed using both signs for the LOS velocities. The second method computes the LOS velocity using the relative velocity of the sources through the ISM obtained from our model fitting (see Sects. 4.2, 5.1). With this method we determined an allowed 3-$\sigma$ range of LOS velocities. Furthermore, this approximation helped us eliminate the degeneracy of sign presented in the derivation of the LOS velocity using the first method. The computed escape velocities, the proper motions, and the 3-$\sigma$ ranges for the LOS velocities are reported in Table 10. The 3D positions and proper motions use a Gaussian distribution as prior, while the LOS velocity uses a uniform distribution. These parameters allowed us to determine the $PDF(a, e, i, \Omega, \omega, P, T_0)$ of each one of our sources.

After obtaining the PDFs of the orbital parameters, we computed the orientation of the sources’ orbital planes in the sky, as viewed from SgrA*. The orientation of the orbital planes can be described by a unitary vector $(\hat{\delta})$ originating at the position of Sgr A* and normal to the source’s orbital plane. To determine the Cartesian components of $\hat{\delta}$, the PDFs of the inclination angle, $i$, and the ascending node, $\Omega$, were used according to the following expression:

$$\hat{\delta} = \left( \begin{array}{c} s_x \\ s_y \\ s_z \end{array} \right) = \left( \begin{array}{c} \sin i \cos \Omega \\ -\sin i \sin \Omega \\ -\cos i \end{array} \right).$$

Figure 11 displays the pointing vectors obtained with the PDFs of the orientation of the sources’ orbital planes using a Hammer projection. The left column of the maps shows the vectors of the PDF($i, \Omega$) of the bow shocks using the computed 3-$\sigma$ LOS range. The right column shows the vectors of the PDF($i, \Omega$) using only the 3-$\sigma$ LOS upper limit determined from the escape velocity. For IRS 10W we only computed its probability distribution using the 3-$\sigma$ LOS upper limit since this source was not clearly identified as a bow shock. Additionally, we included the PDF($i, \Omega$) of IRS 16CC, a source previously studied by Lu et al. (2009), to check the validity of our code. We obtain similar results to those previously published, which confirms the accuracy of our code. Each map in Fig. 11 displays the 1-$\sigma$ and 2-$\sigma$ confidence levels of the PDFs in red and blue. The confidence levels were computed using only orbital solutions tied to Sgr A*. The ellipses plotted in different colors represent the 1-$\sigma$ contour of the orbital planes of some of the main dynamical structures at the GC. Table 11 shows the peak values of the PDFs for the sources identified as bow shocks.

The plots in the left and right columns of Fig. 11 clearly show that the PDFs based on the modeling of the bow-shocks constrain the orbital planes significantly better than those obtained with the constraints from the escape velocities alone. The PDF($i, \Omega$) of IRS 5 is the best constrained. The derived LOS velocity range of IRS 5 fully eliminates the ambiguity in the sign of the LOS velocity. Conversely, IRS 1W exhibits very similar PDFs using both methods. This effect can be explained by the fact that we only took into account orbits gravitationally bound to Sgr A*. Furthermore, most of the IRS 1W bound orbits obtained from our MC simulation have LOS velocities within the 3-$\sigma$ range derived from our bow-shock modeling. From this analysis we also observe that IRS 5 and IRS 21 clearly are not part of the CWS or the CCWS. IRS 1W and IRS 10W are relatively close to the position of the CWS but still on the edge of the CWS 1-$\sigma$ limits. Hence, we cannot establish with certainty whether they are CWS members or not. None of the sources are moving in the same plane of the NA.

6. Discussion and conclusions

The AO facilities and the sparse aperture masking mode of NACO at the ESO VLT allowed us to perform a NIR multiwavelength campaign to study objects with high-angular resolution the struct-
Fig. 11. Distribution of the orbital planes of IRS 5, IRS 1W, IRS 21, IRS 10W, and IRS 16CC. The 1-σ and 2-σ confidence levels are shown in red and blue. The ellipses represent the 1-σ position of the CCW, CCWS, and the NA orbital planes: the NA is represented by the light-blue ellipse (Paumard et al. 2006; Bartko et al. 2009), the green ellipse corresponds to the CWS according to Lu et al. (2009); the red, pink, and orange ellipses display the CWS according to Bartko et al. (2009) for stars at 0.8’’-12’’, 0.8’’-3.5’’, and 7’’-12’’ projected distances, respectively; the purple star represents the position of the CWS for stars at 3.5’’-7’’ projected distance from Sgr A* (Bartko et al. 2009), and the blue ellipse displays the position of the CCWS according to Paumard et al. (2006).
AO observations in science target, like in the case of the GC. Additionally, we used traditional calibrators are too dim or located far away from the poor background estimates, and problems in the PSF stability. It final calibrator. This method allowed us to minimize the noise, ff does not require observations of an o

We used AO-deconvolved and beam-restored images in est and most embedded sources in the central parsec of the GC. We presented a H

We interpreted our observations with 3D steady-state bow-shock models and confirmed that three of them (IRS 5, IRS 1W, and IRS 21) are bow shocks associated with the relative motion of Wolf-Rayet stars through the ISM. Although this conclusion was suggested previously, our models give the best constraints of Wolf-Rayet stars through the ISM. Although this conclusion

shock of two stellar winds, or there may be a chance superpo-

On the other hand, the extended emission around IRS 10W does not appear to trace a bow shock, but may be produced by the shock of two stellar winds, or there may be a chance superpo-

Table 9. Velocities of the NA ISM considering the bow-shock model used in this work, the Paumard et al. (2004), and the Zhao et al. (2009) models.

| Source | $v_{r,\text{ISM-R.A.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-Dec.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-R.A.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-Dec.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-R.A.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-Dec.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-R.A.}}$ [km s$^{-1}$] | $v_{r,\text{ISM-Dec.}}$ [km s$^{-1}$] | P.A.$^\text{ISM}$ | P.A.$^\text{ISM}$ | P.A.$^\text{ISM}$ |
|---|---|---|---|---|---|---|---|---|---|---|---|
| IRS 5 | -136±76 | -143±56 | -0.88±67 | -133±49 | -54±20 | -141±13 | 223±33 | 0.4±207 | 201±8 |
| IRS 1W | -220±48 | -169±94 | -73±49 | -213±69 | -218±13 | -110±13 | 232±16 | 199±19 | 243±15 |
| IRS 10W | -305±74 | 248±54 | -28.54±63 | -187±85 | -44±29 | -225±50 | 310±76 | 189±19 | 191±11 |
| IRS 21 | -123±16 | -331±41 | -127±54 | -325±51 | -275±28 | -250±66 | 200±13 | 201±17 | 228±80 |

Table 10. 3D coordinates and velocities of IRS 1W, IRS 10W, IRS 21, and IRS 5.

| Star | IRS 1W | IRS 5 | IRS 10W | IRS 21 |
|---|---|---|---|---|
| $x$ [arcsec]$^a$ | 5.26±0.009 | 8.62±0.02 | 6.3±0.01 | -2.33±0.001 |
| $y$ [arcsec]$^a$ | 0.616±0.016 | 9.83±0.032 | 5.15±0.02 | -2.69±0.001 |
| $z$ [arcsec]$^a$ | 7.53±1.53 | 3.81±2.66 | 6.43±1.5 | 4.45±1.07 |
| $v_r$ [km s$^{-1}$]$^b$ | 320±29 | 266±7 | 303±13 | 412±30 |
| $v_{r,\text{ISM-R.A.}}$ [km s$^{-1}$]$^b$ | -164±35 | 54±18 | -21±21 | 165±13 |
| $v_{r,\text{ISM-Dec.}}$ [km s$^{-1}$]$^b$ | 309±22 | 26±25 | 216±14 | 57±33 |
| $v_{r,\text{LOS}}$ [km s$^{-1}$]$^c$ | [-18, 18] | [113, 334] | [-307, 307] | [-79, 261] |

a Motion of the ISM and its position angle measured in this work.
b Motion of the ISM and its position angle measured by Paumard et al. (2004).
c Motion of the ISM and its position angle measured by Zhao et al. (2009).

d Projected distances from SgrA$^*$.
e LOS distance from the plane containing SgrA$^*$, using the NA model of Paumard et al. (2004).
f 3D escape velocity at the position of the source.
g Proper motion measured in this work.
h 3-$\sigma$ range on the LOS velocity of the bow shocks.
density. These changes produce a rapid magnetic alignment of the grains (Buchholz et al. 2013). From the best-fit bow-shock stand-off distances, we have established that their central sources are massive objects (WR stars) with supersonic stellar wind velocities and strong mass-loss rates. They are therefore short-lived objects and have probably formed during the most recent starburst event at the GC.

One of the main sources of uncertainty in determining the orbital planes of the population of massive stars around the GC is the lack of information of the stellar LOS distances (see e.g., Lu et al. 2009; Yelda et al. 2014). Therefore, their LOS distances are significantly better constrained by the result that the extended emission of our sources are bow-shocks produced by the interaction of the stellar source with the NA. This characteristic, unique in this sources, along with their LOS velocity from our best-fit models, their proper motions and models of the ISM in the NA, allowed us to perform a Monte Carlo analysis of the sources’ orbital planes.

IRS 1W stands out from the other sources because of its unusual morphology (see Sect. 4.6), in particular its long tail, which we expect to trace the relative motion between IRS 1W and NA in the past 50 years. From studying the orbital-plane, we derived that the most probable orbit for this source peaks at and NA in the past 50 years. From studying the orbital-plane, unusual morphology (see Sect. 4.6), in particular its long tail, allowed us to perform a Monte Carlo analysis of the sources’ orbital planes, along with their LOS velocity from our best-fit solution of the stellar source with the NA. This characteristic, unique in these sources, along with their LOS velocity from our best-fit models, their proper motions and models of the ISM in the NA, allowed us to perform a Monte Carlo analysis of the sources’ orbital planes.

The derived orbital planes suggest that our sources are not part of any of the suggested disks of young stars in the GC, but our results are consistent with the most recent detailed work on the orbital distribution of the young stars in the GC by Yelda et al. (2014). These authors suggested that only about 20% of 116 O/WR stars, at a projected distances of 0.8” to 12” from Sgr A*, are part of the CWS. Hence, if our bow shocks were members of the CWS, the number of disk members would be increased by about 20%. However, our results show that the target bow-shock sources probably do not form part of the CWS. Therefore, our results provide new evidence for the complexity of the population of young massive stars in the central parsec of the GC and highlight that the disk members are only a small fraction of the young massive stars around Sgr A*.

Table 11. Maxima of the PDFs orbital planes for the inclination (i) and angle of the line of nodes in the sky (Ω).

| Source | i (deg) | Ω (deg) |
|--------|---------|---------|
| IRS 1W | 132     | 154     |
| IRS 5  | 78      | 37      |
| IRS 21 | 51      | 95      |

a Angle between the orbit and the plane of sky.
b Angle between North and the line of ascending nodes, increasing East of North.

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Appendix A: Proper motion measurements
Fig. A.1. Proper motion measurements. Measured positions vs. time in right ascension and declination offsets from Sagittarius A* for the bow-shock sources IRS 1W, IRS 5, IRS 2L, IRS 10W, and IRS 21.

Fig. A.2. Proper motion measurements. Measured positions vs. time in right ascension and declination offsets from Sagittarius A* for the stars IRS 16NW and IRS 33N.