Efficient $2^3S$ positronium production by stimulated decay from the $3^3P$ level

M. Antonello, A. Belov, G. Bonomi, R. S. Brusa, M. Caccia, A. Camper, R. Caravita, F. Castelli, G. Cerchiari, D. Comparat, G. Consolati, A. Demetro, L. Di Noto, M. Doser, M. Faní, S. Gerber, A. Gligorova, D. Krasnický, V. Lagomasino, P. Lebrun, C. Malbrunot, S. Mariazzi, S. M. Røhne, F. Guatieri, E. Oswald, V. Petracek, G. Bonomi, M. Caccia, M. Doser, M. Faní, S. Gerber, A. Gligorova, D. Krasnický, V. Lagomasino, P. Lebrun, C. Malbrunot, S. Mariazzi, S. M. Røhne, F. Guatieri, E. Oswald, V. Petracek, G. Bonomi, M. Caccia, M. Doser, M. Faní, S. Gerber, A. Gligorova, D. Krasnický, V. Lagomasino, P. Lebrun, C. Malbrunot, S. Mariazzi, S. M. Røhne, F. Guatieri, E. Oswald, V. Petracek

We investigate experimentally the possibility of enhancing the production of $2^3S$ positronium atoms by driving the $1^3S$ to $3^3P$ and $3^3P$ to $2^3S$ transitions, overcoming the natural branching ratio limitation of spontaneous decay from $3^3P$ to $2^3S$. The decay of $3^3P$ positronium atoms towards the $2^3S$ level has been efficiently stimulated by a 1312 nm broadband IR laser pulse. The dependence of the stimulating transition efficiency on the intensity of the IR pulse has been measured to find the optimal enhancement conditions. A maximum relative increase of $\times(3.1 \pm 1.0)$ in the $2^3S$ production efficiency, with respect to the case where only spontaneous decay is present, was obtained.

PACS numbers: 32.80.Rm, 36.10.Dr, 78.70.Bj

Positronium (Ps) is the neutral matter-antimatter bound state of an electron ($e^-$) and a positron ($e^+$). Ps has two distinct ground states: the singlet $1^3S$ (para-Ps), annihilating into two $\gamma$-rays with a lifetime of 0.125 ns, and the triplet $1^3S$ (ortho-Ps), annihilating into three $\gamma$-rays with a lifetime of 142 ns [1]. Ps, being a purely leptonic two-body system, is well-known for offering an ideal testing ground for high-precision Quantum Electrodynamics (QED) calculations [2]. Among the many precision experiments, the most accurate were recently conducted using two-photon Doppler-free laser spectroscopy of the $1^3S$ to $2^3S$ transition [3]. The $2^3S$ level has an extended lifetime of $1142 \pm 5$ ns in vacuum. This is due to its optical metastability: single-photon radiative decays to $1^3S$ are prohibited by the electric dipole selection rules and the reduced overlap between the positron and the electron wave-functions increases its annihilation lifetime by a factor of eight [4]. On top of its high-precision spectroscopy applications, $2^3S$ Ps is one of the few notable candidate systems being considered for measuring the gravitational interaction between matter and antimatter [5], together with Ps in long-lived Rydberg states [6, 7].
antihydrogen [8,10] and muonium [11]. Moreover, the metastable 2S Ps has a very low electrical polarizability, thus being scarcely sensitive to stray electric fields [12], and is a good candidate for atom interferometry, provided that a beam with sufficiently low divergence and high intensity is demonstrated [13]. Furthermore, an intense source of polarized 2S atoms has been recently shown to be of extreme usefulness to achieve Bose-Einstein condensation of Ps [13].

2S Ps sources have been demonstrated via RF transition from laser-excited 3P Ps in a weak magnetic field [14], via two-photon Doppler-free 1S–2S laser excitation [15,16] and more recently via single-photon excitation of 1S to 2P in a rapidly switching electric field [17] and via single-photon excitation of 1S to 3P with radiative decay to 2S in an electric field [18] and in absence of electric field [19]. This last method in particular showed that it is possible to build an almost-monochromatic 2S Ps source with a selected and tunable velocity distribution in the 10⁴ m s⁻¹ range, with an overall efficiency between 0.7–1.4% according to the selected velocity [19].

In the present work, following this experimental line, we investigate the possibility of stimulating the 3P–2S transition to increase the overall 2S production efficiency. Indeed, laser-excited 3P Ps can spontaneously decay radiatively to 2S via the dipole-allowed 3P–2S transition (rate A_{23} = 2π×1.1·10⁹ s⁻¹) with ~10% measured branching efficiency [18,19], limited by the competition with the more efficient spontaneous decay channel 3P–1S (A_{13} = 2π×8.4·10⁹ s⁻¹). Increasing the 3P–2S transition rate, and thus the branching efficiency of the 2S decay, is possible through stimulated emission.

A straightforward way to stimulate the 3P–2S transition consists in introducing a synchronized broadband IR laser pulse at 1312.2 nm [5] on top of the pulsed UV laser at ~205 nm used for 1S–3P excitation [20]. In our experiment, such a laser pulse could be obtained from the same optical setup producing the UV beam, which is described in [21,22]. In this setup, a sequence of non-linear optical conversion processes are used to generate the 205 nm wavelength, and in particular an optical parametric generation (OPG) crystal yields as a byproduct a broadband, amplified idler beam at 1314 nm. Both 205 nm and 1314 nm wavelengths could be tuned by varying the temperature set-point of the OPG crystal around its nominal working point of T₁ = 175.6 °C (Fig. 1). This temperature value, chosen for the UV wavelength to fall on the 1S–3P resonance (λ₃ = 205.045 nm), is ineffective for a stimulated emission experiment as the bandwidth of the IR does not arrive to cover the 1312.2 nm wavelength with sufficient optical power to efficiently stimulate the 3P–2S transition. Hence, a different set-point T₂ = 172.4 °C was selected to gain enough power at 1312.2 nm, while maintaining an acceptable detuning δν₃ of the UV beam from the 1S–3P resonance frequency, to minimize the unavoidable reduction in excitation efficiency. The set-point setting accuracy was limited to 0.5 °C by the TC200 temperature controller. At T₂, the induced 1S–3P detuning was δν₃ = 410 GHz, corresponding to 205.103 nm and 0.9σ of the Doppler distribution of our Ps source (σₙ ≈ 470 GHz [20]). A reduction in the 1S–3P excitation efficiency of about ~50% was expected [29], due to the Doppler selection of a Ps atoms distribution with λ₃δν₃ ≈ 0.85·10⁸ m s⁻¹ average velocity in the direction parallel to the laser beam.

A direct way to observe an enhancement in the 2S signal due to the action of the stimulating laser is to compare the Ps annihilation time distribution with the UV laser only to that measured with both UV and IR pulses. The experimental methodology was the same used in previous works [18,20]. Bursts of 10⁷ e⁺, 7 ns in time length [23], were guided by a 25 mT magnetic field, focused by an electric field of about 300 V cm⁻¹ and implanted at 3.3 keV in a circular spot of ~3 mm full-width at half maximum (FWHM) into a e⁺/Ps converter held at room temperature. The converter is constituted by a Si(111) p-type crystal with nanochannels produced via electrochemical etching and oxidized in air at 100 °C for 2 h [23]. Ps formed in the converter out-diffuses back into vacuum through the nanochannels with
an efficiency up to 35% loosing a fraction of its for-
formation energy by collisions with the channel walls [25]. A fraction of the emitted cloud was subsequently con-
voyed to 2S either by the 205 nm UV beam alone (i.e. through spontaneous decay from 3P, as in [18, 19]) or by a combination of the UV and IR laser pulses (i.e. through stimulated decay from 3P). Both beams were linearly polarized perpendicularly to the target, with a nearly Gaussian temporal profile with a FWHM of 1.5 ns (UV) and 4.0 ns (IR), and a nearly-Gaussian spectral pro-
file with bandwidths \( \sigma_{\text{UV}} \approx 2 \pi \times 120 \text{ GHz} \) (UV) and \( \sigma_{\text{IR}} \approx 2 \pi \times 440 \text{ GHz} \) (Fig. 1). The energy of the two pulses was \((53 \pm 5) \mu \text{J}\) for the UV and \((405 \pm 10) \mu \text{J}\) for the IR (at the entrance viewpoint of the experimental chamber). The UV spot was nearly Gaussian with \((7.0 \pm 0.7) \text{ mm}\) FWHM both in horizontal and vertical directions, while the IR spot was uniform in power and slightly astigmatic, \((12.9 \pm 0.5) \times (17.2 \pm 0.5) \text{ mm}\) FWHM in the horizontal and vertical directions, due to a geometrical cut of an optical element. Two spurious light backgrounds at 532 nm and 894 nm were found superimposed to the 1312 nm beam with the same spot size, caused by the non-ideality of the dichroic mirrors used to separate the beams, with energies \(\approx 80 \mu \text{J}\) and \(\approx 100 \mu \text{J}\) respectively. Photo-ionisation of 2S or 3P due to these backgrounds was negligible due to their low intensities and the small photo-ionisation cross-sections \((10^{-16} \div 10^{-17} \text{ cm}^2)\). As the presence of an electric field would have shorten considerably the optical longevity of 2S Ps [19], a fast HV switch with a rise time < 15 ns was used to disable the guiding electric field of the focusing electrode (see Fig. 2-a) \(\sim 5\) ns after \(e^+\) imprint-
plantation [19], such that the field was negligible when the excitation lasers were shot \((\sim 20\text{ ns after } e^+ \text{ implanta-
tion})\).

The time distribution of the annihilation \(\gamma\) rays due to the implanted \(e^+\) and decaying/annihilating Ps was mea-
sured with a \(20 \times 25 \text{ mm}\) lead tungstate (PbWO\(_4\)) scin-
tillator [26] coupled to a Hamamatsu R11265-100 photo-
multiplier tube (PMT), placed 40 mm above the Ps con-
verter. The signal from the PMT was 50%-50% split and digitized using two channels of a HD4096 Teledyne LeCroy 2.5Gs oscilloscope set at high \((100 \text{ mV/Div})\) and low \((1 \text{ V/Div})\) gains to further extend the linear dynamic range of the digitizer. The data of the two channels were joined to form the so-called single-shot positron an-
nihilation lifetime spectroscopy (SSPALS) spectra [27], whose average is proportional to the amount of \(\text{Ps}/e^+\) an-
nihilating per unit time. The total lifetime of 2S Ps in absence of an electric field \((1142 \text{ ns})\) is longer than that of 1S \((142 \text{ ns})\) and of all other populated sub-
levels in the \(n = 1 - 3\) manifolds. Thus, an increase in the delayed annihilations (either due to in-flight or to pick-off annihilations as the Ps atoms hit the cham-
ber walls) for \(t \gg 142 \text{ ns}\) (t being the time elapsed from \(e^+\) implantation) can be directly related to the amount of 2S Ps (as in [19]). Relative time-dependent varia-
tions between two SSPALS spectra families with different laser configurations were quantified using the parameter \(S(t) = (A_1(t) - A_2(t))/A_1(t)\) where \(A_1(t), A_2(t)\) are the (averaged) integrated areas below single SSPALS shots of the two families in a selected time window centered in \(t\). In this definition \(A_1(t)\) has the role of the reference area. An alternating measurement scheme between the two families was used to minimize the effect of time drifts of the experimental conditions. Contributions of event-
tual residual long-time drifts in the \(S\) calculation were further reduced by normalizing the shots in each family to a second-order polynomial fit of their value versus time (detrending technique, see [18] App.).

Figure 2: a) Distributions of Ps impact positions, shown superimposed to the 3D drawing of the chamber walls, for the \(T_1 = 175.6 \text{ °C}\) (blue circles) and \(T_2 = 172.4 \text{ °C}\) (red circles) setpoints, emphasizing the different Doppler selection in the two detuning conditions. b) Measurement of the annihilation time distributions of spontaneously-decaying 2S Ps atoms from the 3P level without stimulated transition into 2S for the two temperature set-points. The graph shows the curve \(S(t) = (A_{\text{UV}}(t) - A_{\text{off}}(t))/A_{\text{off}}(t)\) (see text). Each time distribution has been fitted with the Monte Carlo model discussed in the text (solid lines).

First, a set of reference spontaneous 2S Ps pro-
duction measurements was acquired on the detuned OPG set-point \((T_2)\) to measure the \(S(t) = (A_{\text{off}}(t) - \)
the $A^{UV}(t)/A^{off}(t)$ parameter in the absence of stimulated emission in the conditions selected for the following experiments. The measured $S(t)$ curve was compared to one acquired at the on-resonance set-point ($T_1$) (see Fig. 2), which was well characterized previously [19]. $A^{UV}$ and $A^{off}$ correspond to the integrated averaged areas with and without the UV laser. Time windows of 300 ns width with steps of 50 ns were used to calculate $S(t)$. All measurements were obtained alternating shots with the UV laser to the same number without it ($\sim 200$ shots for $T_1$, $\sim 300$ shots for $T_2$). The peak of $2^{3}$S annihilations on the chamber walls is more evident in the on-resonance ($T_1$) measurement (between 500 ns and 750 ns) than in the detuned ($T_2$) measurement, where it is lower and smeared to longer times, in agreement with a reduced $2^{3}$S production efficiency and longer atoms’ traveled distances, because of the Doppler selection operated by the detuned UV beam that selects atoms traveling longer trajectories.

The experimental $S(t)$ curves were fitted using a previously-developed Monte Carlo (MC) model [18, 19]. This MC calculates the atoms’ flight trajectories (starting from our Ps source velocity distribution [20]) and their excitation dynamics by simultaneously integrating the center-of-mass equations of motion and optical rate equations for the internal level dynamics. The annihilation position/time distribution for $1^{3}$S and $2^{3}$S Ps in flight and by collisions with the chamber walls [18] are calculated. The only fitting parameter was the $1^{3}$S–$3^{3}$P excitation efficiency $\eta_3$, while the $2^{3}$S branching $\eta_m$ ($=0.097$) and quenching $\eta_q$ ($=0.17$) efficiencies were set according to past measurements (with the same laser delay of 20 ns, see [19]). Different Doppler selections in the two set-points were now constrained to the measured UV detunings (0 GHz for $T_1$ and 410 GHz for $T_2$).

The fit (Fig. 2 solid lines) yielded $\eta_3 = (12.4 \pm 0.7)\%$ for $T_1$ and $\eta_3 = (5.2 \pm 0.4)\%$ for $T_2$, corresponding to a $\approx 58\%$ reduction in the excitation efficiency as a consequence of the UV laser detuning, in agreement with the expected $\sim 50\%$ [20]. The annihilations’ position distributions resulting from the fit (Fig. 2a) emphasize the difference in the atoms’ flight trajectories in the chamber geometry in the two different detuning conditions.

Subsequently, the 1312.2 nm IR pulse was introduced to stimulate the $3^{3}$P–$2^{3}$S transition. A first measurement campaign to optimize the IR laser $2^{3}$S production efficiency was carried out by progressively attenuating its energy from the nominal 405 µJ with a set of graded neutral density filters. The idea behind this optimization search is that the desired stimulated emission from the $3^{3}$P level competes dynamically with the repumping of this level by absorption from the $2^{3}$S. This mainly depends on the pulse energy (maintaining the other pulse parameters, in particular the FWHM temporal profile). One expects that on our nanosecond time scale, while a low energy can induce only a low population gain on the $2^{3}$S level, a too high energy subtracts population from that previously efficiently excited by the rising part of the pulse. The optimization measurements were acquired alternating ($\sim 200$) shots with both UV and IR lasers to shots with UV laser only. Their associated $S(t) = (A^{UV}(t) - A^{UV+IR}(t))/A^{UV}(t)$ reflected the relative signal changes only caused by the IR, i.e. isolating the effects of this laser pulse (resonant with the $3^{3}$P–$2^{3}$S transition) on the $2^{3}$S Ps population. The resulting $S(t)$ curves (an example of which - with 5 dB attenuation - is shown in Fig. 3 inset) exhibit an excess of annihilations in the region around 550 ns and 1050 ns, where the impact of $2^{3}$S atoms onto the chamber walls is also observed in the reference measurement ($T_2$ in Fig. 3). A convenient way to show the enhancement in the $2^{3}$S production is to consider a total $\bar{S}$ parameter calculated in the wide time window 550-1050 ns, normalized on the total parameter $\bar{S}$ of the reference measurement (calculated in the same time window). The results are reported in Fig. 3 as a function of the 1312.2 nm laser pulse attenuation.

The effect of the 1312.2 nm laser is compatible with zero when the beam is sent with full power. Then the effect progressively increases as the laser energy is decreased to reach a maximum at 5 dB attenuation ($E_{peak} \approx 126 \mu J$) to slowly decrease again at even higher attenuations.

![Figure 3: The ratio $\bar{S}/\bar{S}_0$ between the total $S$ parameters, as defined in the text, versus the attenuation in dB of the IR laser pulse starting from the maximum energy 405 µJ (black points): Top inset: the $-S(t)$ parameter in the case of the 5 dB attenuation point.](image-url)
ation (where $E_{\text{peak}} \sim 126 \mu \text{J}$), to slowly decrease again at even higher attenuations. These measurements indicate that, selecting the 1312.2 nm laser pulse energy at $E_{\text{peak}}$, an increase of $(190 \pm 90)\%$ (corresponding to a $\times(2.9 \pm 0.9)$ gain efficiency) in the amount of produced $2^3\text{S}$ with respect to the reference was obtained.

A final measurement campaign was conducted to directly evaluate the $2^3\text{S}$ branching efficiency achieved by setting the 1312.2 nm laser to the optimal energy. The set of measurements was acquired alternating ($\sim 200$) shots with both UV and IR lasers to shots with both lasers off. The resulting $S(t) = (A^{\text{off}}(t) - A^{\text{UV+IR}}(t))/A^{\text{off}}(t)$ curve, compared to the reference $2^3\text{S}$ curve obtained in the same temperature set-point $T_2$ and in the absence of the IR enhancement laser (previously plotted in Fig. 2), is shown in Fig. 4. The $2^3\text{S}$ branching efficiency was evaluated by fitting $-S(t)$ with the Monte Carlo model. The fit was now performed letting $\eta_m$ vary, while keeping all other parameters fixed to those determined in the reference measurement. The found value for the branching efficiency was $\eta^{\text{UV}}_m = 0.297\pm0.019$. This value, compared to the branching efficiency previously estimated from the measurement with the UV laser alone with the same laser delay ($\eta^{\text{UV}}_m = (0.097 \pm 0.027)$ [19]), leads to a $2^3\text{S}$ Ps enhancement of $\times(3.1 \pm 1.0)$, in perfect agreement with the IR pulse optimization measurement.

In conclusion, we experimentally demonstrated the possibility to efficiently stimulate the $3^1\text{P}$--$2^3\text{S}$ transition of Ps by employing a pulsed, broadband 1312.2 nm laser. The highest enhancement efficiency was found by tuning the intensity of the IR laser pulse inducing the $3^1\text{P}$--$2^3\text{S}$ transition. In these optimal conditions of our experiment, due to the pulsed excitation dynamics, the relative enhancement of the $2^3\text{S}$ Ps atoms production from the excited $2^3\text{S}$ population, with respect to the reference of the spontaneous emission decay, was measured to be $\times(3.1 \pm 1.0)$. This corresponds to a branching efficiency of $2^3\text{S}$ production from the $3^1\text{P}$ level that can be up to $\sim 30\%$. Anyway, the overall $2^3\text{S}$ Ps excitation efficiency was limited by the present technical restriction in producing both pulsed laser beams with the correct wavelengths and energies using a single optical parametric generation stage. The variation in the temperature set-point of the laser generation crystal, necessary to output the correct 1312.2 nm wavelength with sufficient energy, induced an UV detuning of about 410 GHz and a reduction in the amount of excited $3^1\text{P}$ of $\approx 58\%$.

In a future realization of this experiment, the present technical limitations could be overcome by separating the two UV and IR laser lines, i.e. having independent nonlinear optical generation and amplification stages. An advantage of having the two laser wavelengths independent from each other would be to retain the full tunability characteristics of our $2^3\text{S}$ source [19], while conveying $\sim 30\%$ of what could be excited to $3^1\text{P}$ to $2^3\text{S}$. Furthermore, if one accepts to sacrifice the mentioned velocity selection, a further increase up to a factor of five of the overall excitation efficiency could be obtained by enlarging the UV laser bandwidth to cover efficiently the Ps Doppler profile. Finally, the first laser spectroscopy of the $3^1\text{P}$--$2^3\text{S}$ transition would become feasible. A laser system with independent UV and IR laser lines is currently under development to take full advantage of this $1^3\text{S}$--$3^1\text{P}$--$2^3\text{S}$ stimulated excitation scheme in view of future measurements on a beam $2^3\text{S}$ Ps.

The authors are grateful to Dr. S. Cialdi for the original development of the $1^3\text{S}$--$3^1\text{P}$ laser. This work was supported by Istituto Nazionale di Fisica Nucleare; the CERN Fellowship programme and the CERN Doctoral student programme; the Swiss National Science Foundation Ambizione Grant (No. 154833); a Deutsche Forschungsgemeinschaft research grant; an excellence initiative of Heidelberg University; Marie Skłodowska-Curie Innovative Training Network Fellowship of the European Commission’s Horizon 2020 Programme (No. 721559 AVA); European Research Council under the European Unions Seventh Framework Program FP7/2007-2013 (Grants Nos. 291242 and 277762); European Union’s Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement ANGRAM No. 748826; Austrian Ministry for Science, Research, and Economy; Research Council of Norway; Bergen Research Foundation; John Templeton Foundation; Ministry of Education and Science of the Russian Federation and Russian Academy of Sciences and the European Social Fund within the framework of realizing the project.
in support of intersectoral mobility and the European Social Fund within the framework of realizing Research infrastructure for experiments at CERN, LM2015058.

* Corresponding author, ruggero.caravita@cern.ch

[1] A. Rich, Rev. Mod. Phys. 53, 127 (1981).
[2] S. G. Karshenboim, Phys. Rep. 422, 1 (2005).
[3] D. B. Cassidy, Eur. Phys. J. D 72, 53 (2018).
[4] M. Charlton and J. W. Humberston, Positron Physics (Cambridge University Press, 2001).
[5] M. K. Oberthaler, Nucl. Instr. Meth. Phys. Res. B 192, 129 (2002).
[6] A. P. Mills and M. Leventhal, Nucl. Instr. Meth. Phys. Res. B 192, 102 (2002).
[7] D. B. Cassidy and S. D. Hogan, International Journal of Modern Physics: Conference Series 30, 1450259 (2014).
[8] C. Amole et al., Nat. Commun. 4, 1785 (2013).
[9] S. Aghion et al. (AEgIS collaboration), Nat. Commun. 5, 4538 (2014).
[10] P. Perez et al. (GBAR collaboration), Hyperfine Interact. 233, 21 (2015).
[11] A. Antognini et al., Atoms 6, 17 (2018).
[12] T. E. Wall, A. M. Alonso, B. S. Cooper, A. Deller, S. D. Hogan, and D. B. Cassidy, Phys. Rev. Lett. 114, 173001 (2015).
[13] Y. Zhang, M.-S. Wu, J.-Y. Zhang, Y. Qian, X. Gao, and K. Varga, arXiv p. 1903.08353 (2019).
[14] A. P. Mills, S. Berko, and K. F. Canter, Phys. Rev. Lett. 34, 1541 (1975).
[15] S. Chu, A. P. Mills, and J. L. Hall, Phys. Rev. Lett. 52, 1689 (1984).
[16] M. S. Fee, A. P. Mills, S. Chu, E. D. Shaw, K. Danzmann, R. J. Chichester, and D. M. Zuckerman, Phys. Rev. Lett. 70, 1397 (1993).
[17] A. M. Alonso, S. D. Hogan, and D. B. Cassidy, Phys. Rev. A 95, 033408 (2017).
[18] S. Aghion et al. (AEgIS collaboration), Phys. Rev. A 98, 013402 (2018).
[19] C. Amsler et al. (AEgIS collaboration), Phys. Rev. A 99, 033405 (2019).
[20] S. Aghion et al. (AEgIS collaboration), Phys. Rev. A 94, 012507 (2016).
[21] S. Cialdi, I. Boscolo, F. Castelli, F. Villa, G. Ferrari, and M. Giammarchi, Nucl. Instrum. Methods Phys. Res. B 269, 1527 (2011).
[22] R. Caravita, Master’s thesis, Università degli Studi di Milano (2013).
[23] S. Aghion et al. (AEgIS collaboration), Nucl. Instrum. Methods Phys. Res., Sect. B 362, 86 (2015).
[24] S. Mariazzi, P. Bettotti, S. Larcheri, L. Toniutti, and R. S. Brusa, Phys. Rev. B 81, 235418 (2010).
[25] S. Mariazzi, P. Bettotti, and R. S. Brusa, Phys. Rev. Lett. 104, 234401 (2010).
[26] D. B. Cassidy and A. P. Mills, Nucl. Instr. Meth. Phys. Res. A 580, 1338 (2007).
[27] D. B. Cassidy, S. H. M. Deng, H. K. M. Tanaka, and A. P. Mills, Appl. Phys. Lett. 88, 194105 (2006).