Clustering, Anisotropy, Spectra of Ultra High Energy Cosmic Ray: Finger-prints of Relic Neutrinos Masses in Dark Halos

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The Ultra High Energy Cosmic Ray (UHECR), by $\nu_r$-Z showering in Hot Dark Halos (HDM), should exhibits an energy spectra and an anisotropy reflecting (also) the relic neutrino masses and their hierarchical HDM halo clustering. The lighter are the relic $\nu$ masses, the higher their corresponding Z resonance energy peaks and their hadronic UHECR tails, the wider their dark halos and the smaller their clustering density contrast (and their interaction probability). A twin light neutrino mass splitting may reflect to twin Z resonance and into a complex UHECR spectra modulation (a twin bump) at the edge at highest GZK energy cut-off. Each possible $\nu$ mass associates a characteristic dark halo size (galactic, local, super cluster) and its local anisotropy due to our peculiar position within that dark matter distribution. The expected Z or WW,ZZ showering into $p\bar{p}$ but also $n\bar{n}$ should imprint a peculiar matter-anti matter symmetry in observed UHECR clustering. A $\nu$ HDM halo around a Mpc will allow to the UHECR $n\bar{n}$ secondary component at $E_n > 10^{20}$ eV (due to Z decay) to arise playing a role comparable with the charged $p\bar{p}$ ones. Their un-deflected $n\bar{n}$ (or decayed $p\bar{p}$) flight is shorter leading to a prompt and hard UHECR trace pointing toward the original UHECR source direction. The direct $p\bar{p}$ pairs are split and spread by random magnetic fields into a more diluted and smeared UHECR signal around the original source direction. TeVs signals by synchrotron radiation must also mark the Z-WW Showering. The UHE $\nu_r$-Z showering signatures may be already found in recent (and future) events in AGASA (and Auger) data. The observed hard doublet and triplets spectra, their time and space clustering already favour the rising key role of UHECR $n\bar{n}$ secondaries originated by $\nu_r$-Z tail shower.

KEYWORDS: Cosmic Ray, Neutrinos Mass, Dark Halos

§1. Introduction

Neutrino with a light mass may play a relevant role in solving the puzzle of Hot Dark Matter within a hot-cold dark matter (HCDM) scenario. At the same time their clustering in Galactic, Local dark halos offer the possibility to overcome the Greisen Zatsepin Kuzmin cut-off ($\gtrsim 4 \cdot 10^{19}$ eV) (GZK) at highest energy cosmic ray astrophysics. These rare events almost in isotropic spread are probably originated by blazars AGN, QSRs in standard scenario, and they should not come, if originally of hadronic nature, from large distances because of the electromagnetic dragging friction of cosmic 2.75 K BBR and of the lower energy diffused inter-galactic radio backgrounds. Indeed as noted by Greisen, Zatsepin and Kuzmin,\(^1\),\(^2\) proton and nucleon mean free path at $E > 5 \cdot 10^{19}$ $EeV$ is less than 30 $Mpc$ and asymptotically nearly ten $Mpc$; also gamma rays at those energies have even shorter interaction length ($10Mpc$) due to severe opacity by electron pair production via microwave and radio background interactions.\(^3\) Nevertheless these powerful sources (AGN, Quasars, GRBs) suspected to be the unique source able to eject such UHECRs, are rare at nearby distances ($\lesssim 10 \div 20 Mpc$, as for nearby $M87$ in Virgo cluster); moreover there are not nearby AGN in the observed UHECR arrival directions. Strong and coherent galactic\(^3\) or extragalactic\(^4\) magnetic fields, able to bend such UHECR (proton, nuclei) directions are not really at hand. The needed coherent lengths and strength are
not easily compatible with known cosmic data on polarized Faraday rotation. Finally in latter scenario the same contemporaneous ultra-high energy ZeV neutrons born, by photopion production on BBR, may escape the magnetic fields bending and should keep memory of the primordial nearby (let say M87) arrival direction, leading to (unobserved) in-homogeneities toward the primary source. Finally secondaries EeV photons (by neutral pion decays) should also abundantly point and cluster toward the same nearby AGN sources,\(^5\)\(^6\) contrary to (never observed) AGASA data. Another solution of the present GZK puzzle, the Topological defects (TD), assumes as a source, relic heavy particles of early Universe; they are imagined diffused as a Cold Dark Matter component, in galactic or Local Group Halos. Nevertheless the TD fine tuned masses and ad-hoc decays are unable to explain the growing evidences of doublets and triplets clustering in AGASA UHECR arrival data. In this scenario there have been recent suggestions\(^7\) for an unexpected population of such 500 compact dark clouds of \(10^3 M_\odot\), each one made by such dark TD clusters, spread in our galactic halo; these dark clouds are assumed nevertheless, not correlated to luminous known galactic halo, disk, globular clusters and center components. We found all these speculations not plausible. On the other side there are possible evidences of self-correlation between UHECR arrival directions with far Compact Blazars\(^16\) at cosmic distance well above GZK cut-off.\(^13\)

Therefore the solution of UHECR puzzle based on primary Extreme High Energy (EHE) neutrino beams (from AGN) at \(E_\nu > 10^{21}\) eV and their undisturbed propagation from cosmic distances up to nearby calorimeter (made by relic light \(\nu\) in dark galactic or local dark halo\(^9\)\(^10\)\(^11\)\(^12\)) is still, in our opinion, the most favorite conservative solution for the GZK puzzle. Interestingly new complex scenarios for each neutrino mass spectra are then opening and important signature of UHECR Z,WW showering must manifest in observed anisotropy and space-time clustering.

§2. UHE neutrino scattering on \(\nu_\tau\) neutrino masses

If relic neutrinos have a mass larger than their thermal energy (1.9 \(K^0\)) they may cluster in galactic or Local Group halos; at eVs masses the clustering seem very plausible and it may play a role in dark hot cosmology.\(^8\)

Their scattering with incoming extra-galactic EHE neutrinos determine high energy particle cascades which could contribute or dominate the observed UHECR flux at GZK edges. Indeed the possibility that neutrino share a little mass has been reinforced by Super-Kamiokande evidence for atmospheric neutrino anomaly via \(\nu_\mu \leftrightarrow \nu_\tau\) oscillation. An additional evidence of neutral lepton flavour mixing has been very recently reported also by Solar neutrino experiment (SNO,Galley,K2K). Consequently there are at least two main extreme scenario for hot dark halos: either \(\nu_\mu, \nu_\tau\) are both extremely light \((m_{\nu_\mu} \sim m_{\nu_\tau} \sim \sqrt{(\Delta m)^2} \sim 0.05 eV)\) and therefore hot dark neutrino halo is very wide and spread out to local group clustering sizes (increasing the radius but loosing in the neutrino density clustering contrast), or \(\nu_\mu, \nu_\tau\) may share degenerated (eV masses) split by a very tiny different values. In the latter fine-tuned neutrino mass case \((m_\nu \sim 0.4eV - 1.2eV)\) (see Fig.2 and Fig.3) the Z peak \(\nu_\tau \bar{\nu}_\tau\) interaction\(^9\)\(^10\)\(^11\)\(^12\) will be the favorite one; in the second case (for heavier non constrained neutrino mass \((m_\nu \gtrsim 3eV))\) only a \(\nu_\tau \rightarrow W^+W^-\)\(^9\)\(^10\) and the additional \(\bar{\nu}_\tau \rightarrow ZZ\) interactions, (see the cross-section in Fig.1)\(^14\) considered here will be the only ones able to solve the GZK puzzle. Indeed the relic neutrino mass within HDM models in galactic halo near \(m_\nu \sim 4eV\), corresponds to a lower and \(Z\) resonant incoming energy

\[
E_\nu = \left( \frac{4eV}{\sqrt{m_\nu^2 + p_\nu^2}} \right) \cdot 10^{21} eV.
\]

This resonant incoming neutrino energy is unable to overcome GZK energies while it is showering mainly a small energy fraction into nucleons \((p, \bar{p}, n, \bar{n})\), (see Tab.1 below), at energies \(E_p\) quite below. (see Tab.2 below).

\[
E_p = 2.2 \left( \frac{4eV}{\sqrt{m_\nu^2 + p_\nu^2}} \right) \cdot 10^{19} eV.
\]

Therefore too heavy (> 1.5eV) neutrino mass are not fit to solve GZK by \(Z\)-resonance while WW,ZZ showering as well as t-channel showering may naturally keep open the solution. In particular the overlapping of both the
Z and the WW, ZZ channels described in fig.1, for $m_\nu \lesssim 2.3\,\text{eV}$ while solving the UHECR above GZK they must pile up (by Z-resonance peak activity) events at $5\cdot 10^{19}\,\text{eV}$, leading to a bump in AGASA data. It is indeed a first marginal evidence of such a UHECR bump in AGASA and Yakutsk data that may stand for this interpretation. More detailed data are needed to verify such conclusive possibility. Similar result regarding the fine tuned relic mass at $0.4\,\text{eV}$ and $2.3\,\text{eV}$, (however ignoring the WW ZZ and t-channels and invoking very hard UHE neutrino spectra) have been independently reported recently.\(^{15}\)

Most of us consider cosmological light relic neutrinos in Standard Model at non-relativistic regime neglecting any relic neutrino momentum $p_\nu$ term. However, at lightest mass values the momentum may be comparable to the relic mass; moreover the spectra may reflect additional relic neutrino-energy injection which are feeding standard cosmic relic neutrino at energies much above the same neutrino mass. Indeed there may exist, within or beyond Standard Cosmology, a relic neutrino component due to stellar, Super Nova, GRBs, AGN past activities, presently red-shifted into a KeV-eV spectra, piling into a relic neutrino grey-body spectra. Therefore it is worth-full to keep the most general mass and momentum term in the target relic neutrino spectra. In this windy ultra-relativistic neutrino cosmology, eventually leading to a neutrino radiation dominated Universe, the halo size to be considered is nearly coincident with the GZK one defined by the energy loss length for UHECR nucleons ($\sim 20\,\text{Mpc}$). Therefore the isotropic UHECR behaviour is guaranteed but a puzzle related to uniform source distribution seem to persist. Nevertheless the UHE neutrino- relic neutrino scattering do not allow a flat spectra as shown in figure 2, (as well as any hypothetical $\nu$ grey body spectra). This leave open the opportunity to have a relic relativistic neutrino component at eVs energies as well as the observed non uniform UHECR spectra. This case is similar to the case of a very light neutrino mass much below 0.1 eV.

As we noticed above, relic neutrino mass above a few eVs in HDM halo are not consistent with naive Z peak; higher energies interactions ruled by WW,\(^{10,23}\) ZZ cross-sections\(^{14}\) may nevertheless solve the GZK cut-off. In this regime there will be also possible to produce by virtual W exchange, t-channel, UHE lepton pairs, by $\nu_\ell \bar{\nu}_j \rightarrow l_i l_j$, leading to additional electro-magnetic showers injection.

As we shall see these important and underestimated signal will produce UHE electrons whose final trace are TeVs synchrotron photons. The hadronic tail of the Z or $W^+W^-$ cascade maybe the source of final nucleons $p, \bar{p}, n, \bar{n}$ able to explain UHECR events observed by Fly’s Eye and AGASA\(^{16}\) and other detectors. The same $\nu_\tau$ interactions are source of Z and W that decay in rich shower ramification. The average energy deposition for both gauge bosons among the secondary particles is summarized in Table 1A below.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Particle & Multiplicity & Energy & $E_{\text{B}}$ & E & $E_{\text{F}}$ (eV) \\
\hline
$Z$ & 2 & 2 & 18 & 18 & 18 \\
$W$ & 2 & 2 & 26 & 26 & 26 \\
$\gamma$ & 2 & 15 & 15 & 15 & 15 \\
$\pi^0$ & 2 & 15 & 15 & 15 & 15 \\
$\nu_\tau$ & 2 & 13 & 13 & 13 & 13 \\
$\nu_\bar{\tau}$ & 2 & 13 & 13 & 13 & 13 \\
\hline
\end{tabular}
\end{table}

Fig. 1. Table 1A: The total detailed energy percentage distribution into neutrino, protons, neutral and charged pions and consequent gamma, electron pair particles both from hadronic and leptonic Z, WW, ZZ channels. We also calculated the electromagnetic contribution due to the t-channel $\nu_\ell \nu_j$ interactions. We used LEP data for Z decay and considered W decay roughly in the same way as Z one. We assumed that an average number of 37 particles is produced during a Z (W) hadronic decay. The number of prompt pions both charged (18) and neutral (9), in the hadronic decay is increased by 8 and 4 respectively due to the decay of $K^0, K^\pm, \rho, \omega, \eta$ particles. (*)We assumed that the most energetic neutrinos produced in the hadronic decay mainly come from charged pion decay. SO their number is roughly three times the number of $\pi$’s. UHE photons are mainly relics of neutral pions. Most of the $\gamma$ radiation will be degraded around PeV energies by $\gamma \gamma$ pair production with cosmic 2.75 K BBR, or with cosmic radio background. The electron pairs instead, are mainly relics of charged pions and will rapidly lose energies into synchrotron radiation. The contribution of leptonic Z (W) decay is also considered and calculated in the table 1A-1B.

\section{UHECR Neutrinos from Z showers}

Although protons (or anti-protons) are the most popular and favorite candidate in order to explain the highest energy air shower observed, one doesn’t have to neglect the signature of final neutron and anti-neutrons as well as electrons...
and photons. Indeed the UHECR neutrons are produced in Z-WW showering at nearly same rate as the charged nucleons. Above GZK cutoff energies UHE $n,\bar{n}$, share a life length comparable with the Hot Galactic Dark Neutrino Halo. Therefore they may be an important component in UHECRs. Moreover prompt UHE electron (positron) interactions with the galactic or extra-galactic magnetic field or soft radiative backgrounds may lead to gamma cascades and from PeVs to TeVs energies.

Gamma photons at energies $E_{\gamma} \simeq 10^{20} - 10^{19}$ eV may freely propagate through galactic or local halo scales (hundreds of kpc to few Mpc) and could also contribute to the extreme edges of cosmic ray spectrum and clustering (see also $^{12,14}$).

The ratio of the final energy flux of nucleons near the Z peak resonance, $\Phi_{p}$ over the corresponding electro-magnetic energy flux $\Phi_{em}$ ratio is, as in tab.1 $e^+e^-,\gamma$ entrance, nearly $\sim \frac{1}{8}$. Moreover if one considers at higher $E_{\nu}$ energies, the opening of WW, ZZ channels and the six pairs $\nu_e\bar{\nu}_\mu$, $\nu_\mu\bar{\nu}_e$, $\nu_e\nu_\tau$ (and their anti-particle pairs) t-channel interactions leading to highest energy leptons, with no nucleonic relics (as $p,\bar{p}$), this additional injection favors the electro-magnetic flux $\Phi_{em}$ over the corresponding nucleon one $\Phi_{p}$ by a factor $\sim 1.6$ leading to $\frac{\Phi_{p}}{\Phi_{em}} \sim \frac{1}{13}$. This ratio is valid at WW, ZZ masses because the overall cross section variability is energy dependent. At center of mass energies above these values, the $\Phi_{p}$ decreases more because the dominant role of t-channel (Fig1). We focus here on Z, and WW,ZZ channels showering in hadrons for GZK events. The important role of UHE electron showering into TeV radiation is discussed below.

As a consequence high energy particle showers are produced in the galactic or local group halo, overcoming the GZK cut-off.$^{10}$ There is an upper bound density clustering for very light Dirac fermions due to the maximal Fermi degeneracy whose adimensional density contrast is $\delta \rho \propto m_\nu^3$, while one finds$^{8}$ that the neutrino free-streaming halo grows only as $\propto m_\nu^{-1}$. Therefore the overall interaction probability grows $\propto m_\nu^2$, favoring heavier non relativistic (eVs) neutrino masses. In this range above few eV neutrino masses only WW-ZZ channel are operative. Nevertheless the same lightest relic neutrinos may share higher Local Group velocities (thousands $\frac{kp}{s}$) or even nearly relativistic speeds and it may therefore compensate the common density bound:

$$n_{\nu_i} = 1.9 \cdot 10^3 \left( \frac{m_i}{0.1 eV} \right)^3 \left( \frac{\nu_{\mu}}{2 \cdot 10^5 \text{km/s}} \right)^3 \quad (1)$$

From the cross section side there are three main interaction processes that have to be considered leading to nucleons in the of EHE and relic neutrinos scattering.

**channel 1.** The $\nu_\tau \rightarrow Z \rightarrow$ annihilation at the Z resonance.

**channel 2.** $\nu_\mu\bar{\nu}_\mu \rightarrow W^+W^-$ or $\nu_\mu\bar{\nu}_\mu \rightarrow ZZ$ leading to hadrons, electrons, photons, through $W$ and $Z$ decay.

**channel 3.** The $\nu_e - \bar{\nu}_e$, $\nu_e - \bar{\nu}_\tau$, $\nu_\mu - \bar{\nu}_\tau$ and antiparticle conjugate interactions of different flavor neutrinos mediated in the t-channel by the W exchange (i.e. $\nu_\mu\bar{\nu}_\tau \rightarrow \mu^+\tau^+$). These reactions are sources of prompt and secondary UHE electrons as well as photons resulting by hadronic $\tau$ decay.

### §4. UHE $\nu - \nu_{\text{relic}}$ Cross Sections

Extragalactic neutrino cosmic rays are free to move on cosmic distances up our galactic halo without constraint on their mean free path, because the interaction length with cosmic background neutrinos is greater than the actual Hubble distance. A Hot Dark Matter galactic or local group halo model with relic light neutrinos (primarily the heaviest $\nu_\tau$ or $\nu_\mu$),$^{10}$ acts as a target for the high energy neutrino beams. The relic number density and the halo size are large enough to allow the $\nu\nu_{\text{relic}}$ interaction.

4.1 The process $\nu_\tau\bar{\nu}_\tau \rightarrow Z$

The interaction of neutrinos of the same flavor can occur via a $Z$ exchange in the s-channel ($\nu_\tau\bar{\nu}_\tau$, and charge conjugated). The cross section for hadron production in $\nu_\tau\bar{\nu}_\tau \rightarrow Z^* \rightarrow$ hadrons is

$$\sigma_Z(s) = \frac{8\pi s}{M_Z^2} \Gamma(Z^* \rightarrow \text{invis.}) \Gamma(Z^* \rightarrow \text{hadrons.}) \quad (2)$$

where $\Gamma(Z^* \rightarrow \text{invis.}) \simeq 0.5 \text{ GeV}$, $\Gamma(Z^* \rightarrow \text{hadrons.}) \simeq 1.74 \text{ GeV}$ and $\Gamma_Z \simeq 2.49 \text{ GeV}$ are respectively the experimental Z width into invisible products, the Z width into hadrons and the
Z full width.\textsuperscript{22)} The averaged cross section peak reaches the value ($\langle \sigma_Z \rangle = 4.2 \cdot 10^{-32} \text{ cm}^2$). We assumed here for a more general case (non relativistic and nearly relativistic relic neutrinos) that the averaged cross section has to be extended over an energy window comparable to half the center of mass energy. The consequent effective averaged cross-section is described in Fig.1 as a lower truncated hill curve.

A $\nu \nu$ interaction mediated in the $s$-channel by the Z exchange, shows a peculiar peak in the cross section due to the resonant Z production at $s = M_Z^2$. However, this occurs for a very narrow and fine-tuned windows of arrival neutrino energies $\nu_i$ (and of the corresponding target neutrino masses and momentum $\bar{\nu}_i$):

$$ E_{\nu_i} = \left( \frac{4eV}{\sqrt{m_{\nu_i}^2 + p_{\nu_i}^2}} \right) \cdot 10^{21} \text{ eV}. \quad (3) $$

So in this mechanism the energy of the EHE neutrino cosmic ray is related to the mass of the relic neutrinos, and for an initial neutrino energy fixed at $E_{\nu} \simeq 10^{22} \text{ eV}$, the Z resonance requires a mass for the heavier neutral lepton around $m_{\nu} \simeq 0.4 \text{ eV}$. Apart from this narrow resonance peak at $\sqrt{s} = M_Z$, the asymptotic behaviour of the cross section is proportional to $1/s$ for $s \gg M_Z^2$.

The $\nu \bar{\nu} \rightarrow Z \rightarrow \text{hadrons}$ reactions have been proposed by\textsuperscript{9,11,12)} with a neutrino clustering on Supercluster, cluster, Local Group, and galactic halo scale within the few tens of Mpc limit fixed by the GZK cut-off. Due to the enhanced annihilation cross-section in the Z pole, the probability of a neutrino collision is reasonable even for a low neutrino density contrast $\delta_{\rho_{\nu}}/\rho_{\nu} \geq 10^2$. The potential wells of such structures might enhance the neutrino local group density with an efficiency at comparable with observed baryonic clustering discussed above. In this range the presence of extended local group halo should be reflected into anisotropy (higher abundance) toward Andromeda, while a much lighter neutrino mass may correspond to a huge halo containing even Virgo and the Super Galactic Plane.

4.2 The $W^+W^-$ and ZZ Channels

The reactions $\nu_\mu \bar{\nu}_\mu \rightarrow W^+W^- \nu_\mu \bar{\nu}_\mu \rightarrow W^{+}W^{-}, \nu_\mu \bar{\nu}_e \rightarrow W^{+}W^{-}$, that occurs through the exchange of a Z boson (s channel),\textsuperscript{23)} has been previously introduced\textsuperscript{10)} in order to explain UHECR as the Fly’s Eye event at 320 Eev detected in 1991 and last AGASA data for a few eV neutrino mass in galactic or local halos. The cross section is given by\textsuperscript{10)}

$$ \sigma_{WW}(s) = \sigma_{\text{asym}} \frac{\beta_W}{2s} \left( \frac{1}{s - M_Z^2} \right) \cdot \{4L(s) \cdot C(s) + D(s)\}. \quad (4) $$

where $\beta_W = (1 - 4M_W^2/s)^{1/2}$, $\sigma_{\text{asym}} = \frac{2s \sin^2 \theta_W M_Z^2}{s M_W^2}$ $\simeq 108.5 \text{ pb}$, and the functions $L(s), C(s), D(s)$ are defined as

$$ C(s) = s^2 + s(2M_{WW}^2 - M_Z^2) + 2M_{WW}^2(M_Z^2 + M_W^2) $$

$$ D(s) = \frac{1}{12M_{WW}^2(s - M_Z^2)} \cdot \left[ s^2(M_Z^4 - 60M_W^4 - 4M_Z^2M_W^2) + 20M_Z^2M_W^2M_Z^2 + 2M_W^4 \right] - 48M_Z^2M_W^4(M_Z^2 + M_W^2). \quad (5) $$

This result should be extended with the additional new ZZ interaction channel considered in\textsuperscript{14)}

$$ \sigma_{ZZ} = \frac{G^2 M_Z^2}{4\pi} \frac{y(1 + \frac{y^2}{2})}{\left( 1 - \frac{y}{2} \right)^2} \cdot \left\{ \ln \frac{2y}{\left( \frac{1 - y}{2} + \sqrt{1 - y} \right)} - \sqrt{1 - y} \right\} \quad (7) $$

where $y = \frac{4 M_Z^2}{s}$ and $\frac{G^2 M_Z^2}{4\pi} = 35.2 \text{ pb}$.

Their values are plotted in Fig.1. The asymptotic behaviour of these cross section is proportional to $\sim \left( \frac{M_Z^2}{s} \right) \ln \left( \frac{s}{M_W^2} \right)$ for $s \gg M_Z^2$.

The nucleon arising from WW and ZZ hadronic decay could provide a reasonable solution to the UHECR events above GZK. We’ll assume that
the fraction of pions and nucleons related to the total number of particles from the W boson decay is the almost the same of Z boson. So W hadronic decay \((P \sim 0.68)\) leads on average to about 37 particles, where \(<n_{\pi^0} \sim 9.19, <n_{\pi^\pm} \sim 17, <n_{\nu,\bar{\nu},\mu,\tau} \sim 2.7\). In addition we have to expect by the subsequent decays of \(\pi^0\)’s (charged and neutral), kaons and resonances \((\rho, \omega, \eta)\) produced, a flux of secondary UHE photons and electrons. As we already pointed out, the particles resulting from the decay are mostly prompt pions. The others are particles whose final decay likely leads to charged and neutral pions as well. As a consequence the electrons and photons come from prompt pion decay. On average it results\(^{22}\) that the energy in the bosons decay is not uniformly distributed among the particles. Each charged pion will give an electron (or positron) and three neutrinos, that will have less than one per cent of the initial W boson energy, while each \(\pi^0\) decays in two photons, each with 1 per cent of the initial W energy. In the Table 1A above we show all the channels leading from single Z, W and Z pairs as well as t-channel in nuclear and electromagnetic components.

4.3 The process \(\nu_i\nu_j \rightarrow l_l l_j\): the t-channel
The processes \(\nu_i\nu_j \rightarrow l_l l_j\) (like \(\nu_\mu\nu_\tau \rightarrow \mu\tau\) for example) occur through the W boson exchange in the t-channel. The cross-section has been derived in,\(^{10}\) while the energy threshold depends on the mass of the heavier lepton produced,
\[
E_{\nu_{l\bar{l}}} = 7.2 \cdot 10^{10}(m_\nu/0.4\ eV)^{-1}(m_\tau/m_{\tau,\mu,e}),
\]
with the term \((m_\tau/m_{\tau,\mu,e})\) including the different thresholds in all the possible interactions: \(\nu_\tau\nu_\mu\) (or \(\nu_\tau\nu_e\)), \(\nu_\mu\nu_\tau\), and \(\nu_e\nu_\tau\). See Fig.2 below.

We could consider as well the reactions \(\nu_\mu\nu_\tau \rightarrow e^-\tau^+, \nu_\tau\nu_\mu \rightarrow e^-\mu^+ \) and \(\nu_e\nu_\tau \rightarrow e^-e^+\), changing the target or the high energy neutrino. Therefore there are 2 times more target than for Z, WW, ZZ channels summarized in Fig.2.

In the ultrarelativistic limit (\(s \simeq 2E_\nu m_\nu \gg M_W^2\)) where \(\nu_\tau\) refers to relic clustered neutrinos) the cross-section tends to the asymptotic value \(\sigma_{\nu_\tau} \simeq 108.5\ pb\).

\[
\sigma_W(s) = \sigma_{\text{asym}} \frac{A(s)}{s} \left\{ 1 + \frac{M_W^2}{s} \right\} \cdot \left[ 2 - \frac{s + B(s)}{A(s)} \ln \left( \frac{B(s) + A(s)}{B(s) - A(s)} \right) \right] \tag{8}
\]

where \(\sqrt{s}\) is the center of mass energy, the functions \(A(s), B(s)\) are defined as
\[
A(s) = \sqrt{[s - (m_\tau + m_\mu)^2][s - (m_\tau - m_\mu)^2]}
\]
\[
B(s) = s + 2M_W^2 - m_\tau^2 - m_\mu^2 \tag{9}
\]
and
\[
\sigma_{\text{asym}} = \frac{\pi\alpha^2}{2\sin^4\theta_W M_W^2} \simeq 108.5\ pb \tag{10}
\]

where \(\alpha\) is the fine structure constant and \(\theta_W\) the Weinberg angle; \(\sigma_{\text{asym}}\) is the asymptotic behaviour of the cross section in the ultrarelativistic limit
\[
s \simeq 2E_\nu m_\nu = 2 \cdot 10^{23} \frac{E_\nu}{10^{22}\ eV} \frac{m_\nu}{10\ eV} eV^2 \gg M_W^2. \tag{11}
\]

This interactions, as noted in Table 1A are leading to electro-magnetic showers and are not offering any nuclear secondary.

§5. The Boosted Z-UHECR spectra
Let us examine the destiny of UHE primary particles (nucleons, electrons and photons) \((E_\nu \lesssim 10^{21}\ eV)\) produced after hadronic or leptonic W decay. As we already noticed in the introduction, we’ll assume that the nucleons, electrons and photons spectra (coming from W or Z decay) after \(\nu\nu\) scattering in the halo, follow a power law that in the center of mass system is \(\frac{dN^*}{dE_{\nu}} \simeq E^{*-\alpha}\) where \(\alpha \sim 1.5\). This assumption is based on detailed Monte Carlo simulation of a heavy fourth generation neutrino annihilations\(^{19,20,21}\) and with the model of quark - hadron fragmentation spectrum suggested by Hill.\(^{24}\)

In order to determine the shape of the particle spectrum in the laboratory frame, we have to introduce the Lorentz relativistic transformations from the center of mass system to the
There are two extreme case to be considered: the case where the interaction occurs at $Z$ peak resonance and therefore the center of mass Lorents factor $\gamma$ is frozen at a given value (eq.1) and the case ($WW, ZZ$ pair channel) where all energies are allowable and $\gamma$ is proportional to $\epsilon^{1/2}$. Here we focus only on $Z$ peak resonance. The consequent fluence spectra $\frac{dN}{d\epsilon^2}$, as above, is proportional to $\epsilon^{-\alpha+2}$. Because $\alpha$ is nearly 1.5 all the consequent secondary particles will also show a spectra proportional to $\epsilon^{1/2}$ following a normalized energies shown in Tab.2, as shown in Fig.(2-6). In the latter case ($WW, ZZ$ pair channel), the relativistic boost reflects on the spectrum of the secondary particles, and the spectra power law becomes $\propto \epsilon^{\alpha/2+1} = \epsilon^{0.25}$. These channels will be studied in details elsewhere. In Fig. 1 we show the spectrum of protons, photons and $e^{-}$ coming from $Z$ hadronic and leptonic decay assuming a nominal primary CR energy flux $\sim 20 \ eV \ s^{-1} \ sr^{-1} \ cm^{-2}$, due to the total $\nu \bar{\nu}$ scattering at GZK energies as shown in figures 2-6. Let us remind that we assume an interaction probability of $\sim 1\%$ and a corresponding UHE incoming neutrino energy $\sim 2000 \ eV \ s^{-1} \ sr^{-1} \ cm^{-2}$ near but below present $UHE$ neutrino flux bound from AMANDA and Baikal as well as Goldstone data.

**SECONDARIES ENERGY DISTRIBUTIONS**

| Channel    | $E(eV)$ | $\frac{dN}{dE} E^2$ (eV) |
|------------|---------|--------------------------|
| $p$        | $2.2 \cdot 10^{20}$ | 1.2                       |
| $\gamma$   | $9.5 \cdot 10^{19}$  | 4.25                      |
| $e_\pi$    | $5 \cdot 10^{19}$  | 2.3                       |
| $e_{prompt}$| $5 \cdot 10^{21}$ | 1.32                      |
| $e_\mu$    | $1.66 \cdot 10^{21}$ | 0.45                      |
| $e_\tau$   | $1.2 \cdot 10^{21}$  | 0.6                       |

Table I. B. Energy peak and Energy Fluence for different decay channels as described in the text. We assumed that in the centre of mass frame, the energy of the proton and of the pion are respectively described in Fig.1 Table 1A.
§6. The UHECRs from Relic $\nu$ Masses

The role of each relic neutrino mass is summarized from the convolutions of the UHE neutrino spectra with the relic neutrino mass, its density as well as the cross-sections described above. The case of Z-resonance event with a single neutrino mass has a narrow fine tuned energy mass windows (0.4 eV-1.2 eV) described respectively in Figures 3-4.

![Fig. 3. Energy Fluence derived by $\nu\bar{\nu}\to Z$ and its showering into different channels: direct electron pairs UHECR nucleons $n, p$ and anti-nucleons, $\gamma$ by $\pi^0$ decay, electron pair by $\pi^+\pi^-$ decay, electron pairs by direct muon and tau decays as labeled in figure. The relic neutrino mass has been assumed to be fine tuned to explain GZK UHECR tail: $m_\nu = 0.1\text{eV}$. The Z resonance ghost (the shadows of Z Showering resonance\textsuperscript{14}) curve), derived from Z cross-section in Fig.1, shows the averaged Z resonant cross-section peaked at $E_\nu = 10^{22}\text{eV}$. Each channel shower has been normalized following table 1B.](image_url)

![Fig. 4. Energy Fluence derived by $\nu\bar{\nu}\to Z$ and its showering into different channels as in previous Figure 2: direct electron pairs UHECR nucleons $n, p$, $\gamma$ by $\pi^0$ decay, electron pair by $\pi^+\pi^-$ decay, electron pairs by direct muon and tau decays as labeled in figure. In the present case the relic neutrino mass has been assumed to be fine tuned to explain GZK UHECR tail: $m_\nu = 1.2\text{eV}$ with the same UHE incoming neutrino fluence of previous figure. The Z resonance curve shows the averaged Z resonant cross-section peaked at $E_\nu = 3.33 \cdot 10^{19}\text{eV}$. Each channel shower has been normalized in analogy to table 1B.](image_url)

We remind again that a heavier neutrino mass ($\geq 2\text{eV/s}$) imply the rise of WW-ZZ channels and a pile up of Z resonance cross-section at lower UHECR spectra. This feature may be already responsible for the tiny bump in observed events around $5 \cdot 10^{19}\text{eV}$. The lighter neutrino mass possibilities (near 0.1 eV) are comparable with present Super-Kamiokande atmospheric neutrino mass and are leading to the exciting scenario where more non degenerated Z-resonances occur.\textsuperscript{14} These scenario are summarized in Fig. 5 (for nominal example $m_{\nu_e} = 0.1\text{eV}$; $m_{\nu_\mu} = 0.05\text{eV}$). The twin neutrino mass inject a corresponding twin bump at highest energy. Another limiting case of interest takes place when the light neutrino masses are extreme, nearly at atmospheric (SK,K2K) and solar (SNO) neutrino masses. This case is described in two different versions in Fig.6 (assuming comparable neutrino densities) and Fig.7 (keeping care of the lightest neutrino density dilutions). The relic neutrino masses are assumed $m_{\nu_e} = 0.05\text{eV}$; $m_{\nu_\mu} = 0.001\text{eV}$). A more complex scenario is also possible when it takes place both a narrow twin bump (Fig5) and a wider twin bump (Fig 6-7) because of a small neutrino tau-muon mass splitting overlapping with a wider one due to lightest neutrino electron mass.

§7. UHECRs Anisotropy and Clustering

The neutrino mass play a role in defining its Hot Dark Halo size and the consequent enhancement of UHECR arrival directions due to our peculiar position in the HDM halo. Indeed for a heavy $\geq 2\text{eV}$ mass case HDM neutrino halo are mainly galactic and/or local, reflecting an isotropic or a diffused amplification toward nearby M31 HDM halo. In the lighter case the HDM should include the Local Cluster up to Virgo. To each size corresponds also a different role of UHECR arrival time. The larger the HDM size the longer the UHECR random-walk travel time (in extra-galactic random magnetic fields) and the wider the arrival rate lag be-
Finger-print of Ultra High Energy Cosmic Ray by Relic Neutrino Masses in Dark Halos

Fig. 5. Energy Fluence derived by $\nu \bar{\nu} \to Z$ and its showering into different channels: direct electron pairs UHECR nucleons $n, p, \gamma$ by $\pi^0$ decay, electron pair by $\pi^+\pi^-$ decay, electron pairs by direct muon and tau decays as labeled in figure. In the present case the relic neutrino masses have been assumed with no degeneracy. Their values have been fine tuned to explain GZK UHECR tail: $m_{\nu_1} = 0.05eV$ and $m_{\nu_2} = 0.08eV$. No relic neutrino density difference has been assumed. The incoming UHE neutrino fluence has been increased by a factor 2 respect previous Fig.3-4. The $Z$ resonance curve shows the averaged $Z$ resonant cross-section peaked at $E_{\nu_1} = 4 \cdot 10^{20}eV$ and $E_{\nu_2} = 8 \cdot 10^{22}eV$. Each channel shower has been normalized in analogy to table 1B.

Fig. 6. Energy Fluence derived by $\nu \bar{\nu} \to Z$ and its showering into different channels as above. In the present extreme case the relic neutrino masses have been assumed with wide mass differences just compatible both with Super-Kamiokande and relic 2K$^o$ Temperature. The their values have been fine tuned to explain observed GZK UHECR tail: $m_{\nu_1} = 0.05eV$ and $m_{\nu_2} = 0.001eV$. No relic neutrino density difference between the two masses has been assumed, contrary to bound in eq.3. The incoming UHE neutrino fluence has been increased by a factor 2 respect previous Fig.2-3. The "$Z$ resonance" curve shows the averaged $Z$ resonant cross-section peaked at $E_{\nu_1} = 8 \cdot 10^{22}eV$ and $E_{\nu_2} = 4 \cdot 10^{24}eV$, just near Grand Unification energies. Each channel shower has been normalized in analogy to table 1B.

between doublets or triplets. The smaller is the neutrino halo the earlier the UHE neutron secondaries by $Z$ shower will play a role: indeed at $E_n = 10^{20}$ eV UHE neutron are flying a Mpc and their directional arrival (or their late decayed proton arrival) are more on-line toward the source. This may explain the high self collimation and auto-correlation of UHECR discovered very recently. The UHE neutrons $Z$-Showering fits with the harder spectra observed in clustered events in AGASA. The same UHECR alignment may explain the quite short (2-3 years) lapse of time observed in AGASA doublets. Indeed the most conservative scenario where UHECR are just primary proton from nearby sources at GZK distances (tens of Mpcs) are no longer acceptable either because the absence of such nearby sources and because of the observed stringent UHECR clustering ($2^\circ - 2.5^\circ$) in arrival direction, as well as because of the short (~3 years) characteristic time lag between clustered events. Finally the same growth with energy of UHECR neutron (and anti-neutron) life-lengths (while being marginal or meaning-less in tens Mpcs GZK flight distances) may naturally explain, within a $\sim Mpc$ Z Showering Neutrino Halo, the arising harder spectra revealed in doublets-triplet spectra.

§8. The Tinyakov-Glushkov Paradox

The same role of UHE neutron secondaries from $Z$ showering in HDM halo may also solve an emerging puzzle: the correlations of arrival directions of UHECRs found recently in Yakutsk data at energy $E = 8 \cdot 10^{18}$ eV toward the Super Galactic Plane are to be compared with the compelling evidence of UHECRs events ($E = 3 \cdot 10^{19}$ eV above GZK) clustering toward well defined BL Lacs at cosmic distances (redshift $z > 0.1 - 0.2$). Where is the real UHECR sources location? At Super-galactic disk (50 Mpcs wide, within GZK range) or at cosmic ($\geq 300 Mpcs$) edges? It should be noted that even for the Super Galactic hypothesis the common proton are unable to justify the high collimation of the UHECR events. Of course both results (or just one of them) maybe
Showering UHECRs. More data will clarify better the real scenario.

§9. The TeV Tails from UHE electrons

As it is shown in Table 1A-B and Figures above, the electron (positron) energies by $\pi^\pm$ decays is around $E_e \sim 2 \cdot 10^{19}$ eV for an initial $E_Z \sim 10^{22}$ eV (and $E_\nu \sim 10^{24}$ eV). Such electron pairs while not radiating efficiently in extra-galactic magnetic fields will be interacting with the galactic magnetic field ($B_G \approx 10^{-6}$ G) leading to direct TeV photons:

$$E_{\gamma}^{\text{sync}} \sim \gamma^2 \left( \frac{eB}{2\pi m_e} \right) \sim$$

$$\sim 27.2 \left( \frac{E_e}{2 \cdot 10^{19} \text{eV}} \right)^2 \left( \frac{m_\nu}{0.4 \text{eV}} \right)^{-2} \left( \frac{B}{\mu\text{G}} \right) \text{TeV.}$$

(14)

The same UHE electrons will radiate less efficiently with extra-galactic magnetic field ($B_G \approx 10^{-9}$ G) leading also to direct peak 27.2 GeV photons. The spectrum of these photons is characterized by a power of law $dN/dEdT \sim E^{-(\alpha+1)/2} \sim E^{-1.25}$ where $\alpha$ is the power law of the electron spectrum, and it is showed in Figures above. As regards the prompt electrons at higher energy ($E_e \sim 10^{21}$ eV), in particular in the t-channels, their interactions with the extra-galactic field first and galactic magnetic fields later is source of another kind of synchrotron emission around tens of PeV energies $E_{\gamma}^{\text{sync}}$:

$$\sim 6.8 \cdot 10^{13} \left( \frac{E_e}{10^{21} \text{eV}} \right)^2 \left( \frac{m_\nu}{0.4 \text{eV}} \right)^{-2} \left( \frac{B}{\mu\text{G}} \right) \text{eV}$$

(15)

$$\sim 6.8 \cdot 10^{16} \left( \frac{E_e}{10^{21} \text{eV}} \right)^2 \left( \frac{m_\nu}{0.4 \text{eV}} \right)^{-2} \left( \frac{B}{\mu\text{G}} \right) \text{eV}$$

(16)

The corresponding energy loss length instead is:

$$\left( \frac{1}{E \frac{dE}{dt}} \right)^{-1} = 3.8 \times \left( \frac{E}{10^{21}} \right)^{-1} \left( \frac{B}{10^{-9}\mu\text{G}} \right)^{-2} \text{kpc.}$$

(17)

a statistical fluctuation. But both studies seem statistically significant (4.6-5 sigma) and they seem in obvious disagreement. There may be still open the possibility of two new categories of UHECR sources both of them located at different distances above GZK ones (the harder the most distant BL Lac sources). But it seem quite unnatural the UHECR propagation by direct nucleons where the most distant are the harder. However our Z-Showering scenario offer different solutions: (1) The Relic Neutrino Masses define different Hierarchical Dark Halos and privileged arrival direction correlated to Hot Relic Neutrino Halos. The real sources are at (isotropic) cosmic edges, but their crossing along a longer anisotropic relic neutrino cloud enhance the interaction probability in the Super Galactic Plane. (2) The nearest SG sources are weaker while the collimated BL Lacs are harder: both sources need a Neutrino Halo to induce the Z-
For the first case the interaction length is few Kpcs while in the second one in few days light flight. Again one has the same power law characteristic of a synchrotron spectrum with index $E^{-(\alpha+1/2)} \sim E^{-1.25}$. Gammas at $10^{16} \div 10^{17}$ eV scatters onto low-energy photons from isotropic cosmic background ($\gamma + BBR \rightarrow e^+e^-$) converting their energy in electron pair. The expression of the pair production cross-section is:

$$\sigma(s) = \frac{1}{2} \pi r_0^2 (1 - v^2)((3 - v^4) \ln \frac{1 + v}{1 - v} - 2v(2 - v^2))$$  \hspace{1cm} (18)$$

where $v = (1 - 4m_e^2/s)^{1/2}$, $s = 2E_\gamma \epsilon(1 - \cos \theta)$ is the square energy in the center of mass frame, $\epsilon$ is the target photon energy, $r_0$ is the classic electron radius, with a peak cross section value at

$$\frac{4}{137} \times \frac{3}{8\pi} \sigma_T \ln 183 = 1.2 \times 10^{-26} \text{cm}^2$$

Because the corresponding attenuation length due to the interactions with the microwave background is around ten kpc, the extension of the halo plays a fundamental role in order to make this mechanism efficient or not. As is shown in Fig.3-4, the contribution to tens of PeV gamma signals by Z (or W) hadronic decay, could be compatible with actual experimental limits fixed by CASA-MIA detector on such a range of energies. Considering a halo extension $l_{halo} \gtrsim 100$kpc, the secondary electron pair creation becomes efficient, leading to a suppression of the tens of PeV signal. So electrons at $E_e \sim 3.5 \cdot 10^{16}$ eV loose again energy through additional synchrotron radiation, with maximum $E_\gamma^{\text{sync}}$ around

$$\sim 79 \left(\frac{E_e}{10^{21} \text{eV}}\right)^4 \left(\frac{m_\nu}{0.4 \text{eV}}\right)^4 \left(\frac{B}{\mu G}\right)^3 \text{MeV}.$$  \hspace{1cm} (19)$$

Anyway this signal is not able to pollute sensibly the MeV-GeV; the relevant signal pile up at TeVs.

Gamma rays with energies up to 20 TeV have been observed by terrestrial detector only by nearby sources like Mrk 501 ($z = 0.033$) or very recently by MrK 421. This is puzzling because the extra-galactic TeV spectrum should be, in principle, significantly suppressed by the $\gamma$-rays interactions with the extra-galactic Infrared background, leading to electron pair production and TeVs cut-off. The recent calibration and determination of the infrared background by DIRBE and FIRAS on COBE have inferred severe constrains on TeV propagation. Indeed, as noticed by Kifune, Protheroe and Meyer we may face a severe infrared background - TeV gamma ray crisis. This crisis imply a distance cut-off, incidentally, comparable to the GZK one. Let us remind also an additional evidence for IR-TeV cut-off is related to the possible discover of tens of TeV counterparts of BATSE GRB970417, observed by Milagrito, being most GRBs very possibly at cosmic edges, at distances well above the IR-TeV cut-off ones. In this scenario it is also important to remind the possibilities that the Fly’ Eye event has been correlated to TeV pile up events in HEGRA. The very recent report (privite communication 2001) of the absence of the signal few years later at HEGRA may be still consistent with a bounded Z-Showering volume and a limited UHE TeV tail activity. To solve the IR-TeV cut-off one may alternatively invoke unbelievable extreme hard intrinsic spectra or exotic explanation as gamma ray superposition of photons or sacrilegious Lorentz invariance violation.

![Fig. 8. Energy fluence by Z showering as in fig.3 and the consequent $e^+e^-$ synchrotron radiation by eq.16-18](image)

§10. Conclusion

UHECR above GZK may be naturally born by UHE $\nu$ scattering on relic ones. The target cosmic $\nu$ may be light and dense as the needed ones in HDM model (few eVs). Then their
The new generation UHECR data within next decade, may also offer the probe of lightest elementary particle masses, their relic densities, their spatial map distribution and energies and the most ancient and evasive shadows of earliest $\nu$ cosmic relic backgrounds.
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