The generation mechanism of spike-and-slow wave discharges appearing on thalamic relay nuclei

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In this paper, we use a model modified from classic corticothalamic network (CT) to explore the mechanism of absence seizures appearing on specific relay nuclei (SRN) of the thalamus. It is found that typical seizure states appear on SRN through tuning several critical connection strengths in the model. In view of previous experimental and theoretical works which were mainly on epilepsy seizure phenomena appearing on excitatory pyramidal neurons (EPN) of the cortex, this is a novel model to consider the seizure observed on thalamus. In particular, the onset mechanism is different from previous theoretical studies. Inspired by some previous clinical and experimental studies, we employ the external stimuli voltage on EPN and SRN in the network, and observe that the seizure can be well inhibited by tuning the stimulus intensity appropriately. We further explore the effect of the signal transmission delays on seizures, and found that the polyspike phenomenon appears only when the delay is sufficiently large. The experimental data also confirmed our model. Since there is a complex network in the brain and all organizations are interacting closely with each other, the results obtained in this paper provide not only biological insights into the regulatory mechanisms but also a reference for the prevention and treatment of epilepsy in future.

Absence epilepsy, a kind of primary generalised seizure diseases, has a strong relationship with the pathological discharge rhythms of bilateral corticothalamic network1, and closely associated with action abort, loss of awareness, muscle rigidity, and behavioural arrest, etc.2,3. Clinically, it is usually characterized by a brief interference in consciousness, along with typical synchronous and bilateral spike-and-wave discharges (SWDs) with slow frequency (approximately 2–4 Hz) on electroencephalography (EEG) of epilepsy patients4,5. This disorder primarily affects children and young adolescents. Although there have been different viewpoints on the origin regions of absence seizures, the exact initial positions are still unknown. Many results have supported the opinion that seizures arise from abnormal interactions among the specific relay nuclei (SRN) of the thalamus, the thalamic reticular nucleus (TRN) and the cerebral cortex structure6–8, which constitute the corticothalamic network (CT). A variety of experimental evidence is presented in Section 8.1 of9. Additionally, the classical clinical electroencephalogram (EEG) waveform often appears in the corticothalamic circuit, especially in the cortex10,11. Many theoretical studies have investigated the mechanism of epilepsy onset in the cortex structure, particularly, by using the mean field model, and the results agree well with the relative experiments12–20.

The thalamus is composed of the TRN and SRN, which play an important role in the production of seizures21,22. The typical epileptic seizure EEG waveform has also been observed on the thalamus in some clinical medical experiments23,24. In addition, many experiments support the theory that disrupting GABAergic inhibition role within the thalamus may be a critical factor to produce abnormal oscillations during seizures25–27. For instance, increased thalamic tonic GABA inhibition has recently been observed in a model28 and in human childhood absence epilepsy29. Seo observed that there are region-specific changes in both phasic and tonic GABA_A subunit expression in the thalamus of an epileptic model, which constitute the corticothalamic network (CT). The thalamus organization has gradually been selected as the target region for deep brain stimulation (DBS), and the control effect was remarkable for some intractable seizures30–34. For example, Klinger

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et al. reviewed the patient outcomes and adverse events related to DBS with various stimulation targets and determined that the DBS may be a safe and effective treatment option for refractory epilepsy. However, there are few theoretical studies that evaluate the generation mechanism of seizures originating from the thalamus directly. Therefore, the underlying physiological processes of these seizures are still unclear, leading to limited understanding of the effect caused by various onset mechanisms.

Another interesting question is whether or not the seizure obtained in the theoretical model can be controlled. As is well known, the brain has a complex network where all organizations closely interact with each other. For instance, the oscillating activity of the basal ganglia (including the substantia nigra pars reticulata (SNr), striatal neurons, globus pallidus tissue and subthalamic nucleus) may exert a great effect on physiological states appearing in CT, especially in epilepsy seizure activity. Recently, Chen et al. reported that absence seizures observed on excitatory pyramidal neurons (EPNs) may be well controlled by tuning the activation level of the SNr and by changing the coupling weight of the direct pallido-cortical pathway. Hu et al. explored the generation mechanism of absence epilepsy appearing on EPN, which is caused by some excitatory pathways projected to the SNR, and they observed that these seizures can be well controlled by appropriately tuning the output from the basal ganglia to the thalamus. Additionally, Hu et al. used an external DBS voltage on the EPN, striatum, SNr and thalamus in a basal ganglia-corticothalamic mean field network and reported that seizures appearing on EPN may be inhibited through changing the period and duration of the current into suitable ranges. However, the controlling problem on seizures in the thalamus has not been involved by now.

Inspired by the previous study, the current study is based on a model modified from the classic CT network. We first evaluate the onset mechanism of seizures appearing on the SNR and then explore the control mechanism by employing external stimuli on the EPN and SNR. We observe that the typical absence seizure may appear on the SNR upon changing several critical coupling strengths and delays in the model. The polyspike wave can only be induced when the delay is sufficiently large. All of seizures can be controlled by tuning the strength of external stimulus appropriately. Through careful analysis, we also find that the TRN could not show obvious attack mechanism in the corticothalamic network and then evaluate the controlling mechanism by using external voltage stimuli on the EPN and SNR. Finally, the effect of the delay on seizures is discussed.

Now, we derive equations to describe the dynamic characteristics of nerve nuclei.

The mean firing rate \( Q_a(t) \) of “a” \((a = s, r, i, e)\) is a sigmoid function of the cell-body potential \( V_a \),

\[
Q_a(t) = \frac{Q_{max}}{1 + \exp \left( - \frac{V_a(t) - \theta_a}{\sigma} \right)}
\]

**Model description and numerical calculation method**

Many previous studies have demonstrated the predictive and descriptive validity of the mean-field approach for modelling a wide range of healthy states as well as generalized seizures in human. We also use the mean-field equation to describe the corticothalamic network. Here, we provide the schematic diagram of the model used in the paper in Fig. 1, which is modified from the classic CT network with four neuronal populations. For simplicity, these populations are denoted as follows: \( s = \) SNR; \( r = \) TRN; \( i = \) inhibitory interneurons (IIN); \( e = \) EPN. We employ different types of lines to represent various projections between populations. Arrow heads represent excitatory inputs mediated by glutamate; round heads represent inhibitory connections regulated by the GABA \(_A\) (solid lines) and GABA \(_B\) (dashed lines) receptors.

![Figure 1. The framework of the CT network. The neural masses are abbreviated as follows: \( r \) = reticular nuclei; \( s \) = specific relay; \( i \) = inhibitory cortical; \( e \) = excitatory cortical. Each box represents a nerve nuclei. Arrow heads represent excitatory inputs mediated by glutamate; round heads represent inhibitory connections regulated by the GABA \(_A\) (solid lines) and GABA \(_B\) (dashed lines) receptors.](image-url)
$Q_{a}^{\text{max}}$ represents the maximum firing rate of “a”, $\theta_e$ represents the mean threshold potential, and $\sigma$ is the standard deviation of firing thresholds. $\overline{\tau}$ is a normalizing parameter obtained by fitting Formula (1) to the error function$^{13}$. It is indicated that the population “a” will discharge at the rate $Q_a$ when the $V_a$ exceeds the $\theta_e$. The sigmoid function can ensure that the firing rate of “a” does not exceed $Q_{a}^{\text{max}}$. It is in line with biological significance, because real neurons cannot fire infinitely quickly.

The variation of the cell-body potential $V_a$ is described by the following differential equations,

$$D_{a,b}V_a(t) = \sum_{b \in B} S(\nu_{ab}) \cdot \nu_{ab} \cdot \phi_b(t)$$

$$D_{a,b} = \frac{1}{\alpha \beta} \left[ \frac{\partial^2}{\partial t^2} + (\alpha + \beta) \frac{\partial}{\partial t} + \alpha \beta \right]$$

$D_{a,b}$ is a differential operator representing dendritic and axon integrals of pulse signals. $\alpha$ and $\beta$ represent the decay and rise rates of $V_a$, $\nu_{ab}$ is the coupling weight in the pathway $b \rightarrow a$. $B$ represents a set of all neural masses projected to “a”. $S(\nu_{ab}) = 1$ means the projection in the pathway $b \rightarrow a$ is excitatory; otherwise, we let $S(\nu_{ab}) = -1$. $\phi_b(t)$ represents the output pulse rate of the mass “b”. Below, we will introduce a delay $\tau$ to describe the slow synaptic kinetics on the pathway “$\text{TRN} \rightarrow \text{SRN}$”, which is induced by the second messenger process.

We employ the following damped wave equation to depict the propagation effect of the axonal field $\phi_a$,

$$\frac{1}{\gamma^2 \tau^2} \frac{\partial^2}{\partial t^2} + 2\gamma \frac{\partial}{\partial t} + \gamma^2 \phi_a(t) = Q_a(t)$$

where $\gamma = \nu / \tau$, is the damping rate of the population, $\nu$ represents the velocity of pulse conduction, and $\tau$ represents the characteristic axonal range. Inhibitory neurons have only short range projections, compared to excitatory neurons$^{12,44}$. Therefore, we suppose that the axons of IIN and TRN are both too short to support pulse conduction; it is suggested that $\phi_a = F(V_a) (d = i, r)$. The pulse propagation effects of EPN and SRN are represented as follows,

$$\frac{1}{\gamma^2 \tau^2} \frac{\partial^2}{\partial t^2} + 2\gamma \frac{\partial}{\partial t} + \gamma^2 \phi_i(t) = Q_i(t)$$

$$\frac{1}{\gamma^2 \tau^2} \frac{\partial^2}{\partial t^2} + 2\gamma \frac{\partial}{\partial t} + \gamma^2 \phi_r(t) = Q_r(t)$$

Because such a large system of DDEs is still computationally expensive, it is naturally desirable to make further simplifications. As suggested by the anatomy of the brain, cortical inhibitory interneurons are relatively sparse compared to pyramidal cells (a ratio of 1:4 in favour of inhibitory interneurons). Therefore, we set $Q_i = Q_r$ and $V_i = V_r$ in our model, as similarly treated in many previous studies$^{12,20,37,40,41}$.

Finally, we rewrote equations (1)–(6) in the first-order form, as delay differential equations, to describe the model in Fig. 1. By implementing this reduction, our model clearly becomes computationally more tractable.

$$\frac{d\phi_a(t)}{dt} = \dot{\phi}_a(t)$$

$$\frac{d\dot{\phi}_a(t)}{dt} = \gamma^2 \cdot \phi_a(t) + F(V_a(t)) - 2\gamma \dot{\phi}_a(t)$$

$$\frac{d\phi_i(t)}{dt} = \dot{\phi}_i(t)$$

$$\frac{d\dot{\phi}_i(t)}{dt} = \gamma^2 \cdot \phi_i(t) + F(V_i(t)) - 2\gamma \dot{\phi}_i(t)$$

$$\frac{dX(t)}{dt} = \dot{X}(t), \ X(t) = \begin{bmatrix} V_i(t), V_j(t), V_k(t) \end{bmatrix}$$

$$\frac{dV_i(t)}{dt} = \alpha \beta \nu_a \phi_k + \nu_e F(V_e) + \nu_a \phi_i(t) - (\alpha + \beta) V_i(t)$$

$$\frac{dV_j(t)}{dt} = \alpha \beta \nu_a \phi_k + \nu_e F(V_e) + \nu_a \phi_j(t) - (\alpha + \beta) V_j(t)$$
Calculation methods of previous studies involving the mean field model of the corticothalamic system were mainly based on the numerical continuation-tools, such as the matlab package DDE-BIFTOOL and PDDE-CONT9,43. In contrast to the study in20,43, all simulations in this paper are performed in the Matlab environment by employing the standard fourth-order Runge-Kutta method, with a integral step of $\Delta t = 0.00005$ s.

First, we performed the bifurcation analysis for several critical coupling strengths to explore the transition mechanism between four states. The bifurcation parameter diagram was obtained by taking the local maximum and minimum values of $\phi_s$ through changing one parameter. All numerical calculations are performed for a sufficient time, and the values taken from the stable time series are adopted. Similarly, we can easily obtain the two-dimensional state bifurcation diagram by adopting the above analysis technology. By using the fast Fourier transform on the time series of $\phi_s$, we can obtain the power spectral density of the SRN. Generally, the spike-wave discharge frequency is the highest at the beginning of the burst and decreases through the seizure, as observed in the experiment. Therefore, we taken the maximum peak frequency as the oscillation dominant frequency in this paper. Unless otherwise noted, all parameter values employed in numerical calculation are listed in the appendix. The external stimuli are small voltages applied on the SRN and EPN directly.

The generation mechanism of seizures by changing several critical coupling strengths

Figure 2A is the bifurcation diagram of $\phi_s$ obtained by varying the coupling strength $v_{es}$. With an increase in $v_{es}$, four states (1)–(4) appear. With each fixed $v_{es}$, a different oscillatory frequency and number of points in the diagram represent four different states. Figure 2B–E are four specific time sequences of $\phi_s$, obtained by setting $v_{es} = 0.6$ mV s, $v_{es} = 1.05$ mV s, $v_{es} = 1.4$ mV s and $v_{es} = 1.8$ mV s, respectively. (F) The linear increase in $v_{es}$. (G) The time series bifurcation diagram of $\phi_s$ with a linear increase in $v_{es}$.
Similarly, we next evaluate the effect of several other critical coupling strengths on the oscillation state of the SRN. Figure 3A presents the bifurcation diagram of $\phi_s$ obtained by varying the coupling strength $v_{se}$. The enhanced strength of $v_{se}$ can increase the activation level of the EPN, which in turn improves the firing level of the SRN. Therefore, states (1), (2), (3) and (4) appear in order with an increase in $v_{se}$. Figure 3B presents the bifurcation diagram of $\phi_s$ obtained by varying the coupling strength $v_{re}$. We set $\tau = 2.7 \text{ s}$ and $v_{se} = 2.4 \text{ mV s}$. (C) The bifurcation diagram of $\phi_s$ obtained by varying the coupling strength $v_{vr}$. We set $-v_{vr} = 1.2 \text{ mV s}$. (E) The bifurcation transition of $\phi_s$ obtained by tuning $v_{re}$. (F) The bifurcation process of $\phi_i$, with increasing in $-v_{se}$. We set $\tau = 0.06 \text{ s}$ and $v_{se} = 2.4 \text{ mV s}$ in (F). (G) The state transition diagram in $(v_{re}, v_{se})$. By varying the parameter values, four states (1)–(4) appeared. (H) Dominant frequency calculation results in the panel $(v_{se}, -v_{se})$. The 2–4 Hz epileptic seizure region is marked as “SWD”, which is surrounded by the white dotted lines. In all simulations of (G,H), we set $v_{se} = 1.2 \text{ mV s}$.

**Inhibit of seizures by using the external stimulation**

An additional question is whether or not the epileptic seizure observed on the SRN can be controlled in our model. As is well known, the seizure is primarily induced by abnormal interactions between the cortex and the thalamus, i.e., the corticothalamic system. Therefore, the epileptic seizure may be regulated by other brain tissues that are closely related to the corticothalamic system, such as the basal ganglia. Considering the anatomical structure of the brain, the globus pallidus externa (GPe) may project the direct GABAergic inhibitory connection to the cortex$^{38,39}$; the SNr demonstrates inhibitory projections to the thalamus by the direct pathway$^{37–42}$ and the indirect pathway$^{43}$, and the subthalamic nucleus (STN) usually has a constant nonspecific input onto the SRN$^{37–42}$. The typical absence seizures appearing on the cortex can be well controlled by these connections to the...
The phenomenon is exhibited by the competition mechanism between S1 and S2. Figure 7A demonstrates the state transition analysis in the plane (−νsr, T). T is the external stimulus voltage applied on TRN. Because T is an excitatory stimulus to the TRN, it can reduce the activation level of SRN. Therefore, the bidirectional control phenomenon is also observed in Fig. 7A by the competition mechanism between C1 and C2. The dominant frequency of seizures falls approximately in the range of 2–4 Hz, easily found in (A). Figure 4B is a typical bifurcation transition of φ1 by setting νsr = 0.4 mV s in Fig. 4A. Here, we set −νsr = 1.2 mV s. (C) A typical transition process of φ1, obtained by setting νsr = 0.4 mV s in (A). (D,E) The dominant frequency of seizures falls approximately in 2–4 Hz, denoted as “SWD” in Fig. 4A, respectively. They show that the changing trend of MFRs is consistent with that in the bifurcation diagram in Fig. 4A.

The SRN enters into the low frequency firing when T is sufficiently large. However, when −νsr is relatively small (less than approximately 1 mV s, as shown in Fig. 7B), the SRN may be in the saturated state or the simple shock state.
Therefore, in this case, the bidirectional control effect appears by tuning T, as indicated by the bidirectional arrow in Fig. 7B.

The effect of the delay $\tau$ on absence seizures

The transmission of signals often has hysteresis effects, especially in inhibitory pathways. As shown in many previous studies involving the epileptic seizure appearing on the EPN13,15,20,37–43, after the GABA$_A$ receptor-induced inhibition begins to inhibit the SRN neurons by the inhibitory pathway “TRN $\rightarrow$ SRN”, we know that they require some time to recovery their firing rates to the rising state in each oscillation period of the SRN. Thus, the next spiking peak can be produced on the SRN when the delay $\tau$ is longer than this restore time, which caused by the GABA$_B$ receptor-induced inhibition. Therefore, the model needs a sufficiently long $\tau$ to guarantee that the generation of SWDs; on the other hand, a longer delay may result in relatively more active firing of the EPN in the second messenger process. In this section, we introduce the delay parameter in the pathways “IIN $\rightarrow$ EPN” and “TRN $\rightarrow$ SRN” to study the effect of $\tau$ on absence seizures observed on the SRN. The model used in this section is shown in Fig. 8, and the revised equations are presented as follows,
\[
\frac{d\phi(t)}{dt} = \dot{\phi}(t)
\]  
(15)

\[
\frac{d\phi(t)}{dt} = \gamma^2[-\phi(t) + F(V_r(t))] - 2\gamma\dot{\phi}(t)
\]  
(16)

\[
\frac{d\phi(t)}{dt} = \dot{\phi}(t)
\]  
(17)

\[
\frac{d\phi(t)}{dt} = \gamma^2[-\phi(t) + F(V_r(t))] - 2\gamma\dot{\phi}(t)
\]  
(18)

\[
\frac{dX(t)}{dt} = \dot{X}(t), \quad X(t) = [V_r(t), V_e(t), V_i(t)]^T
\]  
(19)

\[
\frac{dV_r(t)}{dt} = \alpha\beta\nu_e \phi_e + \nu_i F(V_i) + \nu_e F(V_e(t - \tau_2)) + \nu_i \dot{\phi}_i(t) - V_r(t) - (\alpha + \beta)\dot{V}_r(t)
\]  
(20)

\[
\frac{dV_e(t)}{dt} = \alpha\beta\nu_e \phi_e + \nu_i \dot{\phi}_i(t) - V_e(t) - (\alpha + \beta)\dot{V}_e(t)
\]  
(21)

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**Figure 7.** (A) The state transition analysis in the plane \((-\nu, C)\). C represents the external stimuli on the EPN. (B) The state transition analysis in the panel \((-\nu, T)\). T is the external stimuli applied on the TRN. The seizure may be inhibited by both decreasing and increasing the strength of C or T, as indicated by the bidirectional arrows in A and B.

**Figure 8.** The framework structure of the model modified from Fig. 1. \(\tau_1\) and \(\tau_2\) are two delay parameters on the pathway "TRN \(\rightarrow\) SRN" and "IIN \(\rightarrow\) EPN", respectively.
The control phenomenon is obvious. The control mechanisms are interesting and are different from the previous model. Seizures all can be controlled by the external stimulation acted on EPN, SRN and TRN, and the bidirectional communication may form a resonance system to affect the activity of epilepsy, which supports previous theoretical results. These firing activities may be reduced when transferred from SRN to EPN. Thus, sometimes, the cortex and thalamus have synchronous resonance activities, such as Fig. 12, which also indicate that the amplitude and frequency of spread from the SRN. And, in our simulations, we find that the cortex and thalamus population could appear to differ when the coupling strength between neural populations, or the activation level of different neural populations. Therefore, the seizure appearing in the cortex may be generated independently, or firing activities of neurons through the coupling strength between neural populations, or the activation level of different neural populations. Therefore, the seizure appearing in the cortex may be generated independently, or spread from the SRN. And, in our simulations, we find that the cortex and thalamus population could appear to have synchronous resonance activities, such as Fig. 12, which also indicate that the amplitude and frequency of firing activities may be reduced when transferred from SRN to EPN. Thus, sometimes, the cortex and thalamus may form a resonance system to affect the activity of epilepsy, which supports previous theoretical results. These seizures can all be controlled by the external stimulation acted on EPN, SRN and TRN, and the bidirectional control phenomenon is obvious. The control mechanisms are interesting and are different from the previous model.

Figure 9. (A) The bifurcation diagram of $\phi_1$ by varying the parameter $\tau_1$, $\tau_2$ represents the information transfer delay from the TRN to the SRN, induced by the GABA_A receptor. The state (3) appeared by tuning the $\tau_1$ to approximately 0.16 s. (B–F) Five specific time sequences of $\phi_1$, obtained by setting $\tau_1 = 0.07 \text{s}$, $\tau_1 = 0.18 \text{s}$, $\tau_1 = 0.26 \text{s}$, $\tau_1 = 0.29 \text{s}$ and $\tau_1 = 0.35 \text{s}$, respectively. We observe that the poly-spike wave appears when $\tau_1$ is sufficiently large, such as in Fig. 9D–F. In all simulations, we set $\gamma_{se} = 0.95 \text{ mV s}$, $\nu_{se} = 1.5 \text{ mV s}$, $\gamma = 160 \text{ Hz}$, and $\tau_2 = 0 \text{s}$.

\[
\frac{dV(t)}{dt} = \alpha \beta (\nu_s \phi_1 + \nu_{se} F(V_s) + \nu_{se} G(V(t - \tau_1)) - V(t)) - (\alpha + \beta) V(t)
\]  

(22)

Figure 9A is the bifurcation diagram of $\phi_1$ by varying the parameter $\tau_1$ on the pathway “TRN $\rightarrow$ SRN”. When the $\tau_1$ is larger than 0.16 s, the typical SWDs will appear, such as in Fig. 9C, obtained by setting $\tau_1 = 0.18 \text{s}$. When $\tau_1$ is sufficiently large, the poly-spike waves will appear on the SRN. For example, Fig. 9D is a three-poly-spike wave time sequence diagram obtained by varying the parameter $\tau_1 = 0.26 \text{s}$. Figure 9E is a four-poly-spike wave time sequence diagram obtained by setting $\tau_1 = 0.29 \text{s}$. Figure 9F is obtained by setting $\tau_1 = 0.35 \text{s}$. Figure 10A is the state transition of $\phi_1$ by changing the parameter $\tau_2$ on the pathway “IN $\rightarrow$ EPN”. With increasing $\tau_2$, three states (1), (2) and (3) appear on the SRN. The typical SWDs emerge only when $\tau_2$ is larger than 0.16 s. Figure 10B–E are four specific time sequence diagrams of $\phi_1$, obtained by setting $\tau_2 = 0.02 \text{s}$, $\tau_2 = 0.14 \text{s}$, $\tau_2 = 0.18 \text{s}$ and $\tau_2 = 0.22 \text{s}$, respectively.

Figure 11A is the state bifurcation diagram of $\phi_1$ obtained by varying the parameter $\tau_2$ on the pathway “IN $\rightarrow$ EPN” with relatively large delays. Figure 11B–E are four specific time sequence diagrams of $\phi_1$, obtained by setting $\tau_1 = 0.024 \text{s}$, $\tau_2 = 0.145 \text{s}$, $\tau_1 = 0.3 \text{s}$ and $\tau_2 = 0.8 \text{s}$, respectively. We can see that the poly-spike wave appears when $\tau_2$ is sufficiently large, such as in Fig. 11D, which is a three-poly-spike wave. The SRN shows the period transfer process between the typical absence seizure state and the saturated shock state (PTAS) when $\tau_2$ is further increased, such as in Fig. 11E.

Conclusion

In this paper, we used a model modified from mean-field network composed of the thalamus and cortex to study the mechanism of the absence seizures appearing on the SRN. In this model, the nonspecific subthalamic input onto SRN is omitted, and this does not affect the qualitative dynamical behavior of populations. The axons of SRN neurons are set to be sufficiently long to produce obvious spike waves on SRN, which has not been considered in previous studies. Through numerical calculations, we find that the typical SWDs appear on SRN by tuning all of coupling strengths of the thalamocortical network and the delay on the two inhibitory pathways. The onset mechanism can be well explained from model itself, and we have described it in details in Sections 3–5. Though these similar phenomena also appeared in some previous studies, such as\(^{14,15,20}\), they all considered the seizure appearing in the cortex. But they may have different onset mechanisms, which are studied in this paper. For example, the pathway “TRN $\rightarrow$ SRN” can induce seizures both in our model and in\(^{20}\), but it affects the activity of SRN directly, and affects the activity of cortex indirectly through the pathway “TRN $\rightarrow$ SRN $\rightarrow$ EPN”, which may represent different mechanisms. On the other hand, the change of synaptic connection strengths will affect the firing activities of neurons through the coupling strength between neural populations, or the activation level of different neural populations. Therefore, the seizure appearing in the cortex may be generated independently, or spread from the SRN. And, in our simulations, we find that the cortex and thalamus population could appear to have synchronous resonance activities, such as Fig. 12, which also indicate that the amplitude and frequency of firing activities may be reduced when transferred from SRN to EPN. Thus, sometimes, the cortex and thalamus may form a resonance system to affect the activity of epilepsy, which supports previous theoretical results. These seizures can all be controlled by the external stimulation acted on EPN, SRN and TRN, and the bidirectional control phenomenon is obvious. The control mechanisms are interesting and are different from the previous model.
studies12–20,37–43, which have been discussed details in Section 4. It should also be pointed out that $\nu_{se}$ and $-\nu_{sr}$ are selected as two representative pathways to explore the control mechanism. Moreover, our method can also be extended to control seizures induced by other coupling strengths and delays.

The delay is the critical factor for producing a poly-spike wave. As reported in many previous studies involving the epileptic seizure appearing on the EPN, such as20, and as analyzed in the section of 5, in the second messenger process, the number of pulse extremum points will increase in one period with a longer delay, such as in Fig. 4(a) in20. However, we observed that the minimum delay to produce seizures is larger in the current study ($>0.16$ s) than in20 ($>0.04$ s). As is well known, the output of the TRN affects the activation level of the SRN through the direct inhibitory pathway "TRN $\to$ SRN"; however, it affects the stability of the EPN through the inhibitory pathway "TRN $\to$ SRN" and the excitatory pathway "SRN $\to$ EPN". The signal transmitted from the TRN to the EPN requires a relatively longer time than that from the TRN directly to the SRN. Thus, the delay is required to generate seizures, and it is longer in this paper than in20. Moreover, in this paper, we observed additional complex spike-wave phenomena, such as four-poly-spike-waves. We think that they may be more prone to appear on the SRN than on the EPN; otherwise, when the seizure activity is transferred from the SRN to EPN, the number of poles would decrease. The $GABA_{B}$ receptor pathways have been reported as the basic mechanisms mediating

Figure 10. (A) The state bifurcation diagram of $\phi_s$ obtained by changing the parameter $\tau_2$. $\tau_2$ is the information transfer delay from inhibitory interneurons IIN to the EPN, which may be induced by the $GABA_{B}$ receptor in IIN. The SRN enters the seizure state when $\tau_2$ is increased to approximately 0.15 s. (B–E) Four specific time sequence diagrams of $\phi_s$ are obtained by setting $\tau_2 = 0.02$ s, $\tau_2 = 0.14$ s, $\tau_2 = 0.18$ s and $\tau_2 = 0.22$ s, respectively. In all simulations, we set $-\nu_{sr} = 0.95$ mV s, $\nu_{se} = 1.5$ mV s, $\gamma_s = 160$ Hz, and $\tau_1 = 0$ s.

Figure 11. (A) The bifurcation transition of $\phi_s$ by increasing the parameter $\tau_2$. $\tau_2$ represents the information transfer delay from inhibitory interneurons IIN to the EPN, which may be caused by the $GABA_{B}$ receptor in IIN. (B–E) Four typical time sequence diagrams of $\phi_s$, obtained by setting $\tau_2 = 0.024$ s, $\tau_2 = 0.145$ s, $\tau_2 = 0.3$ s and $\tau_2 = 0.8$ s, respectively. It is shown that the poly-spike wave is produced only when $\tau_2$ is sufficiently large, such as in Fig. 11D,E. We set $-\nu_{sr} = 0.95$ mV s, $\nu_{se} = 1.5$ mV s, $\gamma_s = 160$ Hz, and $\tau_1 = 0$ s in all simulations.
epilepsy seizures in many studies\cite{44,45}. However, after careful investigation, we find that there are few studies on GABA\(_i\) in the cortex inducing absence seizure; thus, we hope that the results obtained in Figs 10, 11 and 12 can inspire further experimental studies.

The source of data employed in simulations has been denoted in appendix. They are all taken in the reasonable biology range, which can also be found in previous studies. For example, the physiologically allowed ranges for \(Q^{\max}_{\alpha}, Q^{\max}_{\beta}, Q^{\max}_{\sigma}\) are 100–1000 Hz\(^{-1}\), and in this model, they are standardized as 250 Hz. The physiological values of \(\theta, \theta, \theta, \theta\) and \(\alpha\) are about 15 mV\(^{-1}\). Generally, the rational biology range of \(\gamma\), is 70–150 Hz\(^{-1}\), and we take it as 100 Hz in our simulations. \(\gamma\) is estimated to be 150 Hz in the model; however, it was not thoroughly evaluated in previous studies. We think this value is reasonable, as referred to the range of \(\gamma\). The time delays are varied by changing the brain environment; unless otherwise noted, we take \(\tau = 0.07\) s in simulations, which is appropriate as described in\cite{30}. \(\alpha, \beta\) and \(\sigma\) are usually set as constants, and the values used in the paper also appeared in previous studies when considering absence epilepsy, such as in\cite{40}. The reasonable biological range of the coupling strengths \(\nu_{ei}, \nu_{ai}, \nu_{ia}, \nu_{se}, \nu_{sr}\) and \(\nu_{se}\) is 0.05–10 mV\(^{-1}\), and hence, we think that these values were reasonably used in this new model.

In\cite{23}, Hu \textit{et al.} first explored the control mechanism of absence epilepsy appearing in the SRN in a corticothalamic-basal ganglia network in which the seizure was induced by the inhibitory pathway “\(\text{TRN} \rightarrow \text{SRN}\)” and inhibited by the basal ganglia. However, as described in the introduction, absence epilepsy seizures are caused by abnormal interactions in the CT network, and accurate onset mechanisms are still unclear. Therefore, in this paper, we first systematically explore the onset mechanism of absence epilepsy seizures appearing in the SRN in a modified CT mean-field network. We find that absence seizures can also be induced by other excitatory and inhibitory pathways in the CT network, which may represent different mechanisms and which have been explained in detail in the paper. It is noted that the effect of delay in the pathway “\(\text{IN} \rightarrow \text{EPN}\)” on seizures has not been involved in previous model studies, the mechanisms of which have been explored in depth in our CT model. Furthermore, we also study the control effect by directly employing the external stimulus voltage on the TRN, SRN and EPN, the mechanism of which has not been discussed in the previous study. Therefore, in this paper, we may provide a unified theoretical framework to study the mechanism of absence seizures appearing in the SRN in the CT model in the future.

It should be noted that the mean-field model is an idealized mathematical model, generally used to facilitate the numerical calculation and to study the qualitative properties of neuron firing activity. The brain environment is very complicated, and several other factors, such as, the synaptic plasticity, the connection structure between neurons, and the delay on excitatory pathways, may all have great influences on seizures in the brain. For example, in our model, we find that the damping rate of the SRN has little effect on seizures (Fig. 13); however, as is well known, the damping rates of different neurons are different and may have important effects on neuronal activity. These studies can only be resorted to the spiking neural network model in the future. Another important question is the control of epileptic seizures. There are many theoretical research results on the control mechanism of epileptic seizures appearing on the cortex by the basal ganglia\cite{27,42}. Although, we have observed some qualitative control mechanisms in our model by employing external stimuli, more refined studies through the internal regulation of the brain need to be conducted in our future studies.

Finally, the main work of the paper is to provide the generation and inhibition mechanisms of absence epilepsy appearing on the SRN, and our model and methods can also be applied to study other types of seizures, such as spasmodic attacks, secondary generalized seizures and juvenile myoclonic epilepsy. They might also be generated on the SRN and have been rarely studied in previous literatures. The transfer between different types of

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**Figure 12.** The synchronous resonance behaviours of SRN and EPN populations, which were obtained by setting \(\nu_{ei} = 0.4\) mV\(^{-1}\), \(\nu_{ai} = 1\) mV\(^{-1}\), \(\nu_{ia} = 1.4\) mV\(^{-1}\) and \(\nu_{se} = 2.5\) mV\(^{-1}\), respectively. They show that the amplitude and frequency of firing activities may be reduced when transferred from the SRN to the EPN.
epileptic seizures may also be an interesting research topic in the future. In light of all the parameters used in the numerical calculation taken from real experimental data, the result obtained in this paper might help us to better understand the mechanism of absence epilepsy appearing in the CT network. On the other hand, in addition to the model-driven approaches described in this paper, data-driven approaches, such as network biomarkers and dynamic network biomarkers based on the high throughput omics data, can also be applied to this field.

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**Figure 13.** The transition process of $\phi$, as the increase of $\gamma_r$. $\gamma_r$ is the damping rate of SRN. We set $-\nu_{\phi_r} = 1.2$ mV s$^{-1}$ in the simulation.
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Author Contributions

B.H., L.C., Y.G. and F.S. conceived the research; B.H. and L.C. wrote the main manuscript text; X.Z., J.D., L.P., M.Y. and C.Z. designed the numerical simulation and data analysis; Z.C., W.T. and H.S. prepared the figures; All authors wrote the paper and approved the final manuscript.

Additional Information

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