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Measurement of dijet azimuthal decorrelation in pp collisions at $\sqrt{s} = 8$ TeV

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Abstract A measurement of the decorrelation of azimuthal angles between the two jets with the largest transverse momenta is presented for seven regions of leading jet transverse momentum up to 2.2 TeV. The analysis is based on the proton-proton collision data collected with the CMS experiment at a centre-of-mass energy of 8 TeV corresponding to an integrated luminosity of 19.7 fb$^{-1}$. The dijet azimuthal decorrelation is caused by the radiation of additional jets and probes the dynamics of multijet production. The results are compared to fixed-order predictions of perturbative quantum chromodynamics (pQCD), and to simulations using Monte Carlo event generators that include parton showers, hadronization, and multiparton interactions. Event generators with only two outgoing high transverse momentum partons fail to describe the measurement, even when supplemented with next-to-leading-order pQCD corrections and parton showers. Much better agreement is achieved when at least three outgoing partons are complemented through either next-to-leading-order predictions or parton showers. This observation emphasizes the need to improve predictions for multijet production.

1 Introduction

Hadronic jets with large transverse momenta $p_T$ are produced in high-energy proton-proton collisions when two partons interact with high momentum transfer via the strong force. At leading order (LO) in perturbative quantum chromodynamics (pQCD), two final-state partons are produced back-to-back in the transverse plane. For this case, the azimuthal angular separation between the two leading $p_T$ jets in the transverse plane, $\Delta\phi_{\text{dijet}} = |\phi_{\text{jet1}} - \phi_{\text{jet2}}|$, equals $\pi$. The nonperturbative effects of multiparton interactions or hadronization disturb this correlation only mildly, and $\Delta\phi_{\text{dijet}} \approx \pi$ still holds. However, the production of a third high-$p_T$ jet leads to a decorrelation in azimuthal angle. The smallest achievable value of $\Delta\phi_{\text{dijet}} = 2\pi/3$ occurs in a symmetric star-shaped 3-jet configuration. Fixed-order calculations in pQCD for 3-jet production with up to four outgoing partons provide next-to-leading-order (NLO) predictions for the region of $2\pi/3 \leq \Delta\phi_{\text{dijet}} < \pi$. If more than three jets are produced, the azimuthal angle between the two leading jets can approach zero, although very small angular separations are suppressed because of the finite jet sizes for a particular jet algorithm. The measurement of the dijet azimuthal angular decorrelation is an interesting tool to gain insight into multijet production processes without measuring jets beyond the leading two.

This paper reports the measurement of the normalized dijet differential cross section as a function of the dijet azimuthal angular separation,

$$\frac{1}{\sigma_{\text{dijet}}} \frac{d\sigma_{\text{dijet}}}{d\Delta\phi_{\text{dijet}}},$$

(1)

for seven regions of the leading jet $p_T$, $p_T^{\text{max}}$, within a rapidity region of $|y| < 2.5$. Experimental and theoretical uncertainties are reduced by normalizing the $\Delta\phi_{\text{dijet}}$ distribution to the total dijet cross section $\sigma_{\text{dijet}}$ within each region of $p_T^{\text{max}}$. For the first time, azimuthal angular separations $\Delta\phi_{\text{dijet}}$ over the full phase space from 0 to $\pi$ are covered. Comparisons are made to fixed-order predictions up to NLO for 3-jet production, and to NLO and LO dijet as well as to tree-level multijet production, each matched with parton showers and complemented with multiparton interactions and hadronization.

The measurement is performed using data collected during 2012 with the CMS experiment at the CERN LHC, corresponding to an integrated luminosity of 19.7 fb$^{-1}$ of proton-proton collisions at $\sqrt{s} = 8$ TeV. Previous measurements of dijet azimuthal decorrelation were reported by the D0 Collaboration in $p\bar{p}$ collisions at $\sqrt{s} = 1.96$ TeV at the Tevatron [1,2], and by the CMS and ATLAS Collaborations in pp collisions at $\sqrt{s} = 7$ TeV at the LHC [3,4].

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2 The CMS detector

A detailed description of the CMS detector, together with a definition of the coordinate system used and the relevant kinematic variables, can be found in Ref. [5]. The central feature of the CMS detector is a superconducting solenoid, 13 m in length and 6 m in inner diameter, providing an axial magnetic field of 3.8 T. Within the field volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL) and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections. Charged particle trajectories are measured by the tracker with full azimuthal coverage within pseudorapidities $|\eta| < 2.5$. The ECAL, which is equipped with a preshower detector in the endcaps, and the HCAL cover the region $|\eta| < 3$. In addition to the barrel and endcap detectors, CMS has extensive forward calorimetry, which extends the coverage up to $|\eta| < 5$. Finally, muons are measured up to $|\eta| < 2.4$ by gas-ionization detectors embedded in the steel flux-return yoke outside the solenoid.

3 Event reconstruction and selection

This measurement uses data samples that were collected with single-jet high-level triggers (HLT) [6]. Four such single-jet HLTs were considered that require at least one jet in the event to have $p_T > 140, 200, 260$, and $320$ GeV, respectively. All triggers were prescaled during the 2012 run except the highest-threshold trigger. The integrated luminosity $\mathcal{L}$ for the four trigger samples is shown in Table 1. The trigger efficiency is estimated using triggers with lower $p_T$ thresholds. Using these four jet-energy thresholds gives 100% trigger efficiencies in the corresponding four momentum regions $200 < p_T^{\text{max}} < 300$ GeV, $300 < p_T^{\text{max}} < 400$ GeV, $400 < p_T^{\text{max}} < 500$ GeV, and $p_T^{\text{max}} > 500$ GeV.

Particles are reconstructed and identified using a particle-flow (PF) algorithm, which combines the information from the individual subdetectors [7,8]. The four-vectors of particle candidates, reconstructed by the above technique, are used as input to the jet-clustering algorithm. Jets are reconstructed using the infrared- and collinear-safe anti-$k_T$ clustering algorithm with a distance parameter $R = 0.7$ [9]. The clustering is performed with the FASTJET package [10] using four-momentum summation.

The reconstructed jets require small additional energy corrections to account for various reconstruction inefficiencies in tracks and clusters in the PF algorithm. These jet energy corrections [11] are derived using (1) simulated events, generated with PYTHIA 6.4.22 [12] with tune Z2* [13,14] and processed through the CMS detector simulation based on GEANT4 [15], and (2) measurements containing dijet, photon+jet, and Z+jet events. The jet energy corrections, which depend on the $\eta$ and $p_T$ of the jet, are applied to the jet four-momentum vectors as multiplicative factors [16]. The overall factor is typically 1.2 or smaller, approximately uniform in $\eta$, and is 1.05 or smaller for jets having $p_T > 100$ GeV. An offset correction is applied to take into account the extra energy clustered into jets from additional proton-proton interactions within the same or neighbouring bunch crossings (in-time and out-of-time pileup) [11]. Pileup effects are important only for jets with low $p_T$ and become negligible for jets with $p_T > 200$ GeV. The current measurement is, therefore, insensitive to pileup effects on jet energy calibration.

Each event is required to have at least one vertex reconstructed offline [17] with a position along the beam line that is within 24 cm of the nominal interaction point. To suppress nonphysical jets, i.e. jets resulting from noise in the ECAL and/or HCAL calorimeters, stringent criteria [18] are applied for identifying jets: each jet should contain at least two particles, one of which is a charged hadron, and the jet energy fraction carried by neutral hadrons and photons should be less than 90%. The efficiency for identifying physical jets using these criteria is greater than 99%.

The two leading jets, which define $\Delta \phi_{\text{dijet}}$, are selected by considering all jets in the event with $p_T > 100$ GeV and an absolute rapidity $|y| < 5$. Events are selected in which the leading jet $p_T$ exceeds 200 GeV and the rapidities $y_1$ and $y_2$ of the two leading jets lie within the tracker coverage of $|y| < 2.5$.

To reduce the background from $t\bar{t}$ and heavy vector boson production, the variable $E_T/\sum E_T$ is used. The sum of the transverse energies is $\sum E_T = \sum_i E_i \sin \theta_i$, and the missing transverse energy $E_T = \sqrt{\sum_i (E_i \sin \theta_i \cos \phi_i)^2 + \sum_i (E_i \sin \theta_i \sin \phi_i)^2}$, where $\theta$ is the polar angle and the sum runs over all PF candidates in the event. A noticeable fraction of high-$p_T$ jet events with large $E_T$ emerges from $t\bar{t}$ production with semileptonically decaying b quarks. In addition, $Z/W$+jet(s) events with $Z$ decays to neutrinos and W decays into charged leptons with neutrinos have high $E_T$ values. The distributions of the variable $E_T/\sum E_T$ are shown in Fig. 1 for the two regions $\Delta \phi_{\text{dijet}} < \pi/2$ (top) and $\pi/2 < \Delta \phi_{\text{dijet}} < \pi$ (bottom). The data (points) are compared to simulated events (stacked), using MADGRAPH 5.1.3.30 [19] matched to PYTHIA6 [12] for event generation. Although some deviations of the simulation with respect to the data are visible in Fig. 1 (cf. Ref. [20]),
(Eq. 1) is corrected for detector smearing effects and unfolded to the level of stable (decay length $c\tau > 1$ cm) final-state particles. In this way, a direct comparison of the measurement with corresponding results from other experiments and with QCD predictions can be made.

The unfolding method is based on the matrix inversion algorithm implemented in the software package ROOUnfold [21]. Unfolding uses a response matrix that maps the distribution at particle-level onto the measured one. The response matrix is derived from a simulation that uses the true dijet cross section distribution from PYTHIA6 with tune Z2* [13] as input, and introduces the smearing effects by taking into account the $\Delta\phi_{dijet}$ resolution. As a cross-check, the response matrix was filled from event samples that have been passed through a detector simulation. No significant difference was observed. The unfolded distributions differ from the raw distributions by 3–4 % for $\Delta\phi_{dijet} < \pi/2$ and by less than 3 % for $\pi/2 < \Delta\phi_{dijet} < \pi$. A two-dimensional unfolding based on the iterative D’Agostini algorithm [22], which corrects for the smearing effects by taking into account both $\Delta\phi_{dijet}$ and $p_T$ resolutions, gives almost identical results.

The main systematic uncertainties arise from the estimation of the jet energy scale (JES) calibration, the jet $p_T$ resolution, and the unfolding correction. The JES uncertainty is estimated to be 1.0–2.5 % for PF jets, depending on the jet $p_T$ and $\eta$ [11,16,23]. The resulting uncertainties in the normalized $\Delta\phi_{dijet}$ distributions range from 7 % at $\Delta\phi_{dijet} \approx 0$ via 3 % at $\pi/2$ to 1 % at $\pi$.

The jet $p_T$ resolution is determined from a full detector simulation using events generated by PYTHIA6 with tune Z2* and is scaled by factors derived from data [11]. The effect of the jet $p_T$ resolution uncertainty is estimated by varying it by one standard deviation up and down, and comparing the $\Delta\phi_{dijet}$ distributions before and after the changes. This results in a variation in the normalized $\Delta\phi_{dijet}$ distributions ranging from 5 % at $\Delta\phi_{dijet} \approx 0$ via 3 % at $\pi/2$ to 0.5 % at $\pi$.

The uncertainty in the unfolding correction factors is estimated by checking the dependence of the response matrix on the choice of the Monte Carlo (MC) generator. An alternative response matrix is built using the HERWIG++ 2.5.0 [24] event generator with the default tune of version 2.3. The observed effect is less than 1 %. An additional systematic uncertainty obtained by varying the $\Delta\phi_{dijet}$ resolution by $\pm 10$ % to determine the unfolding correction factors is estimated to be of the order of 1 %. This variation of the $\Delta\phi_{dijet}$ resolution by $\pm 10$ % is motivated by the observed difference between data and simulation in the $\Delta\phi_{dijet}$ resolution. A total systematic unfolding uncertainty of 1 % accounts for the choice of the MC generator in building the response matrix and the $\Delta\phi_{dijet}$ resolution.

The unfolded dijet cross section differential in $\Delta\phi_{dijet}$ and normalized by the dijet cross section integrated over the entire phase space is shown in Fig. 2 for seven $p_T^{\text{max}}$ regions. Each
Fig. 2 Normalized dijet cross section differential in $\Delta \phi_{\text{dijet}}$ for seven $p_T^{\text{max}}$ regions, scaled by multiplicative factors for presentation purposes. The error bars on the data points include statistical and systematic uncertainties. Overlaid on the data (points) are predictions from LO (dashed line; $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2\pi/3$) and NLO (solid line; $2\pi/3 \leq \Delta \phi_{\text{dijet}} \leq \pi$) calculations using the CT10 NLO PDF set. The PDF, $\alpha_S$, and scale uncertainties are added in quadrature to give the total theoretical uncertainty, which is indicated by the downwards-diagonally (LO) and upwards-diagonally (NLO) hatched regions around the theory lines.

region is scaled by a multiplicative factor for presentation purposes. The $\Delta \phi_{\text{dijet}}$ distributions are strongly peaked at $\pi$ and become steeper with increasing $p_T^{\text{max}}$. Overlaid on the data for $\Delta \phi_{\text{dijet}} > \pi/2$ are predictions from pQCD, presented in more detail in the next section, using parton distribution functions (PDF) of the CT10 PDF set.

5 Comparison to theoretical predictions

5.1 Predictions from fixed-order calculations in pQCD

The theoretical predictions for the normalized dijet cross section differential in $\Delta \phi_{\text{dijet}}$ are based on a 3-jet calculation at NLO. The correction in nonperturbative (NP) effects, which account for multiparton interactions (MPI) and hadronization, is studied using event samples simulated with the PYTHIA6 (tune Z2*) and HERWIG++ (tune 2.3) event generators. Small NP effects are expected, since this measurement deals with a normalized distribution. These corrections are found to be of the order of 1 %, roughly at the limit of the accuracy of the MC simulations. Therefore NP corrections are considered to be negligible and are not applied.

The fixed-order calculations are performed using the NLOJET++ program version 4.1.3 [25,26] within the framework of the fastNLO package version 2.3.1 [27]. The differential cross section is calculated for 3-jet production at NLO, i.e. up to terms of order $\alpha_S^4$, with three or four parts in the final state. This calculation has LO precision in the region $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2\pi/3$ and NLO precision for $2\pi/3 \leq \Delta \phi_{\text{dijet}} \leq \pi$. The bin including $\Delta \phi_{\text{dijet}} = \pi$ is computed from the NLO dijet cross section within this bin. For each region in $p_T^{\text{max}}$, the differential cross section is normalized to the dijet cross section calculated at LO for $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2\pi/3$ and at NLO, i.e. up to terms proportional to $\alpha_S^3$, for $2\pi/3 \leq \Delta \phi_{\text{dijet}} \leq \pi$. The use of the LO dijet cross section for the normalization in the region $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2\pi/3$ leads to an improved description of the data and avoids artificially increased scale uncertainties as described in Refs. [28,29]. Of course, this difference in normalization leads to a discontinuity proportional to $\sigma_{\text{dijet}}^{\text{NLO}}/\sigma_{\text{dijet}}^{\text{LO}}$ at $\Delta \phi_{\text{dijet}} = 2\pi/3$.

The number of quark flavours that are assumed to be massless is set to five, and the renormalization and factorization scales, $\mu_r$ and $\mu_f$, are chosen to be equal to $p_T^{\text{max}}$. The PDF sets with NLO evolutions used in the calculations are tabulated in Table 2. The ABM11 PDF set utilizes a fixed flavour number scheme, whereas the rest of the PDF sets use a variable flavour number scheme. The maximum number of flavours is denoted by $N_f$.

The uncertainties due to the renormalization and factorization scales are evaluated by varying the default choice of $\mu_r = \mu_f = p_T^{\text{max}}$ between $p_T^{\text{max}}/2$ and $2p_T^{\text{max}}$, simultaneously in the differential cross section and in the total cross section, in the following six combinations: $(\mu_r/p_T^{\text{max}}, \mu_f/p_T^{\text{max}}) = (1/2, 1/2), (1/2, 1), (1, 1/2), (1, 2), (2, 1), (2, 2)$. The PDF uncertainties are evaluated according to the prescriptions for the CT10 PDF set in Ref. [35]. The CT10 PDF set employs the eigenvector method with upward and downward variations for each eigenvector. To evaluate the uncertainty due to the value of the strong cou-
Fig. 3 Ratios of the normalized dijet cross section differential in \( \Delta \phi_{\text{dijet}} \) to LO (triangles) and NLO (squares) pQCD predictions using the CT10 PDF set at next-to-leading evolution order for all \( p_T^{\text{max}} \) regions. The error bars on the data points represent the total experimental uncertainty, which is the quadratic sum of the statistical and systematic uncertainties. The uncertainties of the theoretical predictions are shown as inner band (PDF & \( \alpha_S \)) and outer band (scales). The predictions using various other PDF sets relative to CT10 are indicated with different line styles.
highest $p_T^{\text{max}}$ region, where they exceed the data. For smaller $\Delta \phi_{\text{dijet}}$ values between $2\pi/3$ and $5\pi/6$, in particular where the estimate of the theoretical uncertainties becomes small, systematic discrepancies are exhibited that diminish with increasing $p_T^{\text{max}}$. In the 4-jet LO region with $\Delta \phi_{\text{dijet}} < 2\pi/3$, the pattern of increasing deviations towards smaller $\Delta \phi_{\text{dijet}}$ and decreasing deviations towards larger $p_T^{\text{max}}$ is repeated, but with less significance because of the larger scale uncertainty. Similar observations were made in the previous CMS measurement [3], which exhibited larger discrepancies in the 4-jet region due to the normalization to the NLO dijet cross section instead of a LO one.

5.2 Predictions from fixed-order calculations matched to parton shower simulations

The PYTHIA6 [12], PYTHIA8 [37], and HERWIG++ [24] event generators complement LO dijet matrix elements with parton showers to simulate higher-order processes. Both PYTHIA versions, PYTHIA6 with the Z2* tune [13] and PYTHIA8 with the CUETM1 tune [14], employ $p_T$-ordered parton showers [38, 39], while HERWIG++ with the default tune of version 2.3 uses a coherent-branching algorithm with angular ordering of the showers [40].

The MadGraph program version 5.1.5.7 [19] supplies the results of LO matrix element calculations with two to four outgoing partons that can be matched to the implementations of parton showers, hadronization, and MPI of the event generators. In this analysis, it is interfaced with PYTHIA6 with tune Z2* using the MLM matching procedure [41] to avoid any double counting between tree-level and parton shower generated parton configurations.

The Powheg framework [42–44] provides an NLO dijet calculation [45] that can also be matched via the parton showers to event generators. Here, Powheg is used with the CT10NLO PDF set and is interfaced to PYTHIA8 with the CUET [14] tune, which employs the LO CTEQ6L1 [35] PDF set. Predictions with parton showers matched to a NLO 3-jet calculation using Powheg [46] or MadGraph5_AMC@NLO [47] would be even more relevant for a multijet topology. They could not, however, be included within the timescale of this analysis. Approaching azimuthal angular separations close to $\pi$, it might also be interesting to compare to predictions employing the technique of $p_T$ resummation [48].

In Fig. 4 the normalized dijet cross section differential in $\Delta \phi_{\text{dijet}}$ is compared to the predictions from fixed-order calculations supplemented with parton showers, hadronization, and MPI. The error bars on the data points represent the total experimental uncertainty, which is the quadratic sum of the statistical and systematic uncertainties. Figure 5 shows the ratios of these predictions to the normalized dijet cross section differential in $\Delta \phi_{\text{dijet}}$, for the seven $p_T^{\text{max}}$ regions.

The solid band indicates the total experimental uncertainty and the error bars on the MC points represent the statistical uncertainties in the simulated data.

Among the LO dijet event generators PYTHIA6, PYTHIA8, and HERWIG++, PYTHIA8 exhibits the smallest deviations from the measurements. PYTHIA6 and HERWIG++ systemati- cally overshoot the data, particular around $\Delta \phi_{\text{dijet}} = 5\pi/6$. The best description of the measurement is given by the tree-level multiparton event generator MadGraph interfaced with PYTHIA6 for showering, hadronization, and MPI. The Powheg generator (here used only in the NLO dijet mode) matched to PYTHIA8 shows deviations from the data similar to the LO dijet event generators.

6 Summary

A measurement is presented of the normalized dijet cross section differential in the azimuthal angular separation $\Delta \phi_{\text{dijet}}$ of the two jets leading in $p_T$ for seven regions in the leading-jet transverse momentum $p_T^{\text{max}}$. The data set of pp collisions at 8 TeV centre-of-mass energy collected in 2012 by the CMS
experiment and corresponding to an integrated luminosity of 19.7 fb$^{-1}$ is analysed.

The measured distributions in $\Delta \phi_{\text{dijet}}$ are compared to calculations in perturbative QCD for 3-jet production with up to four outgoing partons that provide NLO predictions for the range of $2\pi/3 \leq \Delta \phi_{\text{dijet}} < \pi$ and LO predictions for $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2\pi/3$. The NLO predictions describe the data down to values of $\Delta \phi_{\text{dijet}} \approx 5\pi/6$, but deviate increasingly when approaching the 4-jet region, starting at $\Delta \phi_{\text{dijet}} = 2\pi/3$, particularly at low $p_T^{\text{max}}$. The pattern of increasing deviations towards smaller $\Delta \phi_{\text{dijet}}$ and decreasing deviations towards larger $p_T^{\text{max}}$ is repeated in the 4-jet LO region with $\Delta \phi_{\text{dijet}} < 2\pi/3$, but with less significance because of the larger scale uncertainty.

In a comparison of the normalized $\Delta \phi_{\text{dijet}}$ distributions to the LO dijet event generators PYTHIA6, PYTHIA8, and HERWIG++, PYTHIA8 gives the best agreement. PYTHIA6 and HERWIG++ systematically overshoot the data, particularly for $\Delta \phi_{\text{dijet}} \approx 5\pi/6$. A good overall description of the measurement is provided by the tree-level multijet event generator MADGRAPH in combination with PYTHIA6 for showering, hadronization, and multiparton interactions. The dijet NLO calculations from POWHEG matched to PYTHIA8 exhibit deviations similar to the LO dijet event generators. Improved multijet predictions can be expected from 3-jet NLO calculations matched to parton showers like from POWHEG or MADGRAPH5_AMC@NLO.
Similar observations were reported previously by CMS [3] and ATLAS [4], but with less significance because of the smaller data sets. The extension to $\Delta \phi_{\text{dijet}}$ values below $\pi/2$, the improved LO description in the 4-jet region $\pi/2 \leq \Delta \phi_{\text{dijet}} < 2 \pi/3$, and the comparison to dijet NLO calculations matched to parton showers are new results of the present analysis.

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