Collisional relaxation of vibrational states of SrOH with He at 2 K

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Abstract

Vibrational relaxation of strontium monohydroxide (SrOH) molecules in collisions with helium (He) at 2 K is studied. We find the diffusion cross section of SrOH at 2.2 K to be $\sigma_{d} = (5 \pm 2) \times 10^{-14}$ cm$^2$ and the vibrational quenching cross section for the (100) Sr–O stretching mode to be $\sigma_{q} = (7 \pm 2) \times 10^{-17}$ cm$^2$. The resulting ratio $\eta_{00} = \sigma_{d}/\sigma_{q} \sim 700$ is more than an order of magnitude smaller than for previously studied few-atom radicals (Au et al 2014 Phys. Rev. A 90 032703). We also determine the Franck-Condon factor for SrOH ($\tilde{X}^2 \Sigma^+ \leftarrow \tilde{X}^2 \Sigma^+ (000)$) to be $(4.8 \pm 0.8) \times 10^{-2}$.

1. Introduction

The study and control of cold atom–molecule collisions lies at the interface of physics and chemistry [1–3]. The diversity and complexity of internal molecular structures and molecular interactions provide new possibilities in precision measurement [4, 5], quantum information science [6, 7], condensed-matter physics [8], and controlled chemistry [3]. Detailed understanding of low temperature molecular collisions provides important information necessary for further development of these applications.

Compared to atomic collisions [9], low-temperature collisions of diatomic molecules are much less understood. Recently, however, significant progress has been made [10–12]. Experimental measurements of low energy collisions between simple polyatomic species (like linear triatomics) and atoms can provide crucial input for advancing theoretical models. Supersonic jet beams (sometimes Stark decelerated [13, 14]), atom association [15–17], and buffer-gas cooling [18–20] are the main experimental tools for exploring molecular collisions in the cold (1 K) and ultracold (µK) temperature regimes. The cold, rarefied buffer-gas environment offers a way to study cooling and molecular collisions with precise control of helium buffer-gas density and cell temperature. The efficiency of quenching vibrational motion during the atom–molecule collisional process at low temperature has been recently measured for several systems [21–24].

In this paper, we explore inelastic collisions between strontium monohydroxide (SrOH) and helium ($^4$He) at 2.2 K. Our measurements probe the intermediate range of vibrational energy spacings, compared to previous low temperature collisional results [22–25]. For the excited Sr–O stretching vibrational mode of SrOH, we observe rapid rotational quenching and translational cooling followed by a slower vibrational quenching to the ground vibrational level. Vibrational quenching cross sections are determined with high accuracy. Our work extends the study of vibrational relaxation in cold atom–molecule collisions to linear polyatomic radicals and contributes to an overall physical picture of the dependence of quenching rates on vibrational energy spacing in low energy collisions, providing an important benchmark for theory.

2. Experiment

To create cold SrOH molecules we use laser ablation in combination with buffer-gas cooling [26]. A schematic diagram of the experimental apparatus is shown in figure 1. SrOH ($\tilde{X}^2 \Sigma^+$) molecules are introduced into the gas phase using pulsed Nd:YAG laser ablation at 532 nm of a Sr(OH)$_2$ solid precursor with a pulse energy of $\sim 15 \text{ mJ}$.
and duration of $\sim 5$ ns. We continuously flow $^4$He buffer gas into a 2.5 cm-diameter cell at rates of 0.5–10 standard cubic centimeters per minute (SCCM). The cell is thermally anchored to a pumped helium reservoir at a temperature of $\sim 2.2$ K. The helium density in the cell can be varied between $n_{\text{He}} \approx 1 \times 10^{15} - 1 \times 10^{16} \text{ cm}^{-3}$, resulting in the mean time between molecule-helium diffusive collisions of $\tau \sim 0.6 - 0.06 \mu$s. The typical SrOH density in our experiment is a very small fraction of the helium density $n_{\text{SrOH}} \approx 10^9 \text{ cm}^{-3}$. A detailed description of the cryogenic apparatus used in this experiment is provided by [27].

Laser absorption spectroscopy is performed in the cell to monitor molecule production and thermalization dynamics. SrOH in the ground and excited vibrational levels is detected using $^2\Delta \Pi_{1/2} \leftrightarrow X^2\Sigma^+$ transitions. We use external-cavity diode lasers at 688 nm with a typical detection power of $P \sim 5 \mu W$ and a beam diameter of $\phi \sim 1$ mm. We employ the ‘off-diagonal’ excitation $^2\Delta \Pi_{1/2}(100) \leftrightarrow X^2\Sigma^+(000)$ at 662 nm (25 mW for $\phi \sim 2$ cm) followed by $^2\Delta \Pi_{1/2}(100) \rightarrow X^2\Sigma^+(100)$ spontaneous emission ($\tau_p \approx 30 \text{ ns}$) for optical pumping of ground state molecules into the $X(100)$ state. The relevant energy levels and lasers are shown in figure 2. We use a mechanical shutter to block the optical pumping beam with a closing time $t \leq 150 \mu$s.

### 3. Results and discussion

#### 3.1. SrOH–He diffusion cross section

We determine the SrOH–He diffusion cross section by measuring the time dynamics in the buffer-gas cell of molecules in the $X^2\Sigma^+(000), N = 1$ state, which is the most populated rotational level at 2 K (figure 8). The spectrum of the ground vibrational level of cold SrOH in the first excited rotational level ($N = 1$) is shown in figure 3. The time decay profile of the molecules in the $X(000)$ vibronic state is governed by the diffusion to the walls and pump-out of the cell through the aperture:
\[ \tau_{000} = \tau_d + \frac{1}{\tau_p}, \]  

where \( \tau_{000} \), \( \tau_d \), and \( \tau_p \) are the timescales for the decay of (000) vibrational mode molecules (\( \tau_{000} \)) due to diffusion (\( \tau_d \)) and cell pump-out (\( \tau_p \)). By measuring the on-resonance absorption time profile (figure 4(a)) we can extract the diffusion lifetime of SrOH: 

\[ \tau_d = \left( \frac{1}{\tau_{000}} - \frac{1}{\tau_p} \right)^{-1}. \]

For low buffer-gas flows \( \tau_d/\tau_p < 1 \) [29], and the molecule loss is primarily due to diffusion to the cell walls. Therefore, from our measurements of \( \tau_{000} \) we can directly determine the diffusion lifetime of the molecules in our cell: 

\[ \tau_d \approx \tau_{000}. \]

At long times after laser ablation (\( \geq 10 \) ms), when higher-order diffusion modes have decayed, the in-cell \( \tilde{X} \) (000) population profile is well fitted by a single exponential (figure 4(a)). We determine the SrOH–He momentum transfer cross section by measuring the diffusion lifetime of SrOH (000) mode molecules at different densities of helium buffer gas. From figure 4(b) we find that \( \tau_{000} \) has a linear dependence on the helium density and conclude that (000) mode molecule loss is primarily dominated by diffusion. For a cylindrical cell of length \( L \) and radius \( r \) the time constant of the exponential decay for molecules diffusing through helium gas of density \( n_{He} \) is given by [30]:

\[ \tau_d = \frac{n_{He} \sigma_d}{\bar{v} G}, \]
measured value of \( f_i \) (somewhat larger than previously measured for diatomic molecules). To extract the value of the diffusion cross section, the population in the vibrational mode using the SrOH signal agrees with the theoretical prediction for larger polyatomic molecules.

\[ G = \frac{3\pi}{32} \left( \frac{j_0^2}{\tau^2} + \pi^2 \right), \]  

where \( \nu = \left( \frac{8k_BT}{\pi\mu} \right)^{1/2} \) is the mean SrOH–He collision velocity at temperature \( T \) with reduced mass of the atom–molecule system \( \mu \) and the diffusion cross section \( \sigma_d \) \( (j_0) \approx 2.405 \) is the first root of the Bessel function \( J_0(x) \). From equation (2) we determine that in the diffusive regime \( (\tau_d/\tau_p < 1) \) the in-cell lifetime is directly proportional to the helium density, as seen in our data.

From the measurement of \( \tau_{000} \) as a function of the helium density (figure 4(b)) using equation (2) we can extract the value of the diffusion cross section, \( \sigma_d \approx \tau_{000} \varphi G/n_{He} \), finding the SrOH diffusion cross section in He at 2.2 K to be \( \sigma_d \left( \text{SrOH} - \text{He} \right) = (5 \pm 2) \times 10^{-14} \text{ cm}^2 \). The measured SrOH–He diffusion cross section is somewhat larger than previously measured for diatomic molecules [19, 25] at similar temperatures. The measured value of \( \sigma_d \left( \text{SrOH} - \text{He} \right) \) agrees with the theoretical prediction for larger polyatomic molecules colliding with helium [31].

### 3.2. Vibrational quenching cross sections

Vibrationally excited SrOH molecules are produced during the process of laser ablation. As can be seen from figure 5, vibrationally excited molecules of the (100) \( \text{Sr} \)–O stretching mode quickly (\(<500 \text{ \mu s}\)) thermalize rotationally to \( T_r = 2.8 \pm 0.7 \text{ K} \) and translationally to a temperature \( \approx 5.6 \text{ K} \). We place a bound on the translational temperature from the Doppler fit. Additional linewidth broadening mechanisms are present inside buffer-gas cells as has been seen repeatedly [25]. Vibrational temperature remains out of thermal equilibrium \( (T_r \sim 400 \text{ K}) \) with other degrees of freedom.

In order to populate the \( \tilde{X}(100) \) state we optically pump SrOH molecules from the (000) mode to the (100) vibrational level quickly \((\approx 25 \text{ ms})\) and then decay to the cell translational temperature from the Doppler fit. The optical pumping process increases the population in \( \tilde{X}(100) \) state by an order of magnitude. After the optical pumping laser is turned off, SrOH molecules in the (100) mode decay faster than those in the (000) mode. The optical pumping rate that leads to the faster decay for the (100) molecules is vibrational quenching with timescale \( \tau_q \), using equation (1), we can write the decay rate of the (100) molecules in the buffer-gas cell:

\[
\frac{1}{\tau_{100}} = \frac{1}{\tau_q} + \frac{1}{\tau_d} + \frac{1}{\tau_p},
\]

In the regime where vibrational quenching dominates other loss processes \( (\tau_q \ll \tau_d, \tau_p) \), the measurement of the (100) lifetime gives the quenching time: \( \tau_{100} \approx \tau_q = \left( G_{\text{cell}} m_{He} \right)^{-1} \). As can be seen from figure 7(a), the in-cell lifetime of the molecules in the \( \tilde{X}(100) \) state is inversely proportional to the helium density which indicates that (100) molecule loss is dominated by vibrational quenching.

The dimensionless ratio of elastic to inelastic collision rates \( \Pi_{00} \) indicates the rate of translational versus vibrational equilibration of a molecular sample and can be determined from our measurements by:  

![Figure 5](image-url)
\[ \gamma_{100} = \frac{\tau_0}{\tau_1} = \frac{\sigma q v}{(n_{\text{He}} \tau_q)^{-1}} = \bar{v}^2 G \tau_0 \tau_q, \]

where we used equation (2) in the last step. After extracting lifetimes for the decays of the (000) and (100) vibrational modes (figure 7(b)), we calculate \( \gamma_{100} \) using an approximate form of equation (5):

\[ \gamma_{100} \approx \bar{v}^2 G \tau_{000} \tau_{100} \]

at various buffer-gas densities. The measured value for SrOH(100)–\(^4\)He collisions is \( \gamma_{100} = 680 \pm 80 \) at 2.2 K, i.e. SrOH \( \tilde{X} \) (100) molecules undergo approximately 700 momentum changing collisions before quenching vibrationally.

We can also place an upper bound on \( \gamma_{010} \) for the excited bending mode. The number of collisions necessary for translational cooling of vibrationally excited SrOH molecules produced during laser ablation is given by [32]:

\[ N = -\kappa \ln \left[ \frac{T_f - T_{bg}}{\bar{T}} \right] \approx 100 \]

for \( T_f = 4 \) K, \( T_{bg} = 2 \) K and the coefficient \( \kappa \equiv \{ m_{\text{SrOH}} + m_{\text{He}} \}^2 / \{ 2m_{\text{SrOH}} m_{\text{He}} \} \). Therefore, if \( \gamma > 100 \), the sample will cool translationally and rotationally, before collision-induced vibrational relaxation, leaving a metastable population, as was seen in the (100) mode of SrOH. However, if \( \gamma < 100 \) vibrationally excited molecules will quench before they cool translationally and rotationally. Molecules in the \( \tilde{X}^2\Pi \) (010) vibronic
state were previously detected in supersonic beams for SrOH [33] and CaOH [34] produced using pulsed laser ablation at 300 K. Experimentally, when measuring absorption on the $\Sigma^\Pi_2^\rightarrow +A_X\tilde{0}(010)$ band we saw no evidence of molecules in the excited bending mode. This rapid vibrational thermalization is due to inelastic vibrational collisions with helium. This allows us to place an upper bound $\gamma < 100$, which is consistent with direct experimental measurements for low-lying bending modes in large molecules [24]. In addition to vibrational quenching, there could potentially be other unexpected contributions to the loss of (010) molecules in our experiment like state dependent chemical reactions.

The measured values of $\gamma$ can be used to calculate the absolute values of collisional quenching cross sections:

$$\sigma_\gamma = \frac{\sigma_d}{\gamma}. \quad (8)$$

Combining our measurements of $\gamma$ and $\sigma_d$ we obtain the following values for the vibrational quenching cross sections $\sigma_\gamma(100) = (7 \pm 2) \times 10^{-17}$ cm$^2$ and $\sigma_\gamma(010) > 5 \times 10^{-16}$ cm$^2$.

### 3.3. Rotational thermalization

Rotational thermalization dynamics for SrOH molecules in the (100) and (000) vibrational modes can be extracted by monitoring $\Delta J = \pm 1$ transitions for different rotational levels. From the data shown in figures 5 and 8, we estimate that the rotational temperature thermalizes to $T_\gamma \sim 3$ K within 1 ms after ablation. Since the mean time between collisions is $< 1 \mu$s we conclude that fewer than 1000 collisions are necessary for complete rotational thermalization after laser ablation. The initial rotational temperature following laser ablation process in a similar experiment was measured to be $> 300$ K [35]. Typically, initial translational temperature of species immediately after the ablation process is $\sim 1000$ K [26, 36].

### 3.4. Franck–Condon (FC) factor measurements

Diagonal FC factors are required for scattering thousands of photons necessary for laser cooling or slowing of molecules [37]. Experimental measurements of these factors have focused on diatomic molecules thus far [38–40]. We measure the ratio of FC factors by comparing the ratio of the absorption signals $R_{\text{sig}}$ for $\tilde{A}\Pi_{1/2}(100) \leftrightarrow \tilde{X}^2\Sigma^+(000)$ and $\tilde{A}\Pi_{3/2}(000) \leftrightarrow \tilde{X}^2\Sigma^+(000)$ transitions using $Q_{11}(J^* = 1.5)$ lines shown in figure 9(b). Since the absorption cross section $\sigma$ for a Doppler broadened line in an electronic transition is proportional to the product of the excitation frequency ($\nu$) and FC factor ($q_{\nu \rightarrow \nu'}$) as $\sigma \propto \nu \cdot (q_{\nu \rightarrow \nu'})$ [41],

$$R_{\text{FC}} = \frac{\nu_{000-000}}{\nu_{100-000}} \times R_{\text{sig}}, \quad (9)$$

where $R_{\text{sig}}$ is the ratio of the absorption signals and $\nu$ is the frequency of the corresponding transition. The Born–Oppenheimer approximation and the FC separation of electronic and vibrational motions was applied to the Sr–O stretching mode in the $\tilde{A}$ state of SrOH [41, 42]. We obtain $R_{\text{sig}} = 5.2 \pm 0.2\%$ which gives $R_{\text{FC}} = 5.0 \pm 0.2\%$. Combining our measurement of $R_{\text{FC}}$ with the sum condition $FC_{000-000} + FC_{100-000} \leq 1$,

\[ Also see supplementary material available at stacks.iop.org/njp/17/045003/mmedia.\]

Figure 8. Thermal distribution of rotational levels ($N = J - 1/2$) for the ground vibrational mode (000) of SrOH 1–2 ms after laser ablation. From the Boltzmann distribution fit $y = a(2J + 1)e^{-BJ(J+1)/T}$ ($\beta_{\text{SrOH}} = 0.36$ K), we obtain the rotational temperature $T = 3.5 \pm 0.4$ K.
we obtain the following value for the off-diagonal factor $FC_{000-100} = \left(4.8 \pm 0.2_{\text{stat}} \pm 0.8_{\text{sys}} \right) \times 10^{-2}$. The systematic error contribution is estimated from the laser frequency lock error $\Delta\nu \approx 10$ MHz and using the Doppler lineshape function for the measured linewidth $\Delta\nu_D \approx 40$ MHz. We assume a simple harmonic oscillator model of molecular potentials \cite{43} to estimate $FC_{000-100} \leq 1 \times 10^{-3}$. The extracted value of the diagonal factor $FC_{000-000} = (95.2 \pm 0.8) \times 10^{-2}$ together with the sum condition $FC_{000-000} + FC_{000-100} \leq 1$ lead to a value for the off-diagonal factor $FC_{000-100} = (4.8^{+0.8}_{-0.5}) \times 10^{-2}$. The error in the measured $FC_{000-100}$ accounts for a possible decay to $\tilde{X}(200)$ with the estimated FC factor of $FC_{000-200} \approx FC_{000-100} \approx 1.2 \times 10^{-2}$ in the harmonic oscillator model \cite{43}. Our result indicates that the SrOH $\tilde{A} \rightarrow \tilde{X}$ FC array is highly diagonal, and it should be possible to scatter $\sim 10^3$ photons for SrOH using two lasers ($\lambda_{\tilde{A}(000)\rightarrow \tilde{X}(000)}$ and $\lambda_{\tilde{A}(000)\rightarrow \tilde{X}(100)}$) before the molecules will decay to the $\tilde{X}(200)$ state. In order to determine branching ratios to the excited bending vibrations in the $\tilde{X}$ state a more detailed experimental and theoretical analysis is necessary, which is beyond the scope of this paper. By driving $N' = 0 \rightarrow N'' = 1$ transitions, the rotational loss channel can be eliminated \cite{44}. In addition to the possibility of laser cooling, this may also have important applications for sensitive molecule detection in the magnetic trap environment \cite{45}.

4. Conclusions

Our measurement of the collisional quenching coefficient $\gamma_{00}$ and an upper bound on $\gamma_{10}$ in SrOH–$^4$He collisions provide important information on the interactions between polyatomic molecules and $^4S$-state atoms at temperatures near 1 K. Below we compare our measurements with other experimental values for diatomics in the similar collisional energy regime (multiple-partial waves):

| System          | $\tau$          | $\omega$, cm$^{-1}$ | $T, K$ |
|-----------------|------------------|---------------------|--------|
| NH–$^3$He \cite{22} | $>5 \times 10^4$ | 3093                | 0.6    |
| CaH–$^3$He \cite{25} | $>9 \times 10^3$ | 1258                | 0.5    |
| ThO–$^3$He \cite{23} | $2 \times 10^4$  | 896                 | 1.2    |
| SrOH(100)–$^3$He | 700              | 527                 | 2.2    |
| SrOH(010)–$^3$He | $<100$           | 364                 | 2.2    |

Since SrOH is a relatively heavy molecule with a large density of rovibrational states it is not surprising that vibrational quenching proceeds relatively quickly. Our results indicate that buffer-gas cooling with helium can efficiently thermalize not only translational and rotational but also vibrational degrees of freedom in polyatomic molecules with low frequency vibrational modes ($\omega < 600$ cm$^{-1}$) at timescales $< 1$ ms. Study of SrOH–He cold collisions provides benchmark information on the dependence of vibrational quenching rates on the frequencies of molecular vibrations. The experimental techniques demonstrated in this work can be easily

\footnote{Also see supplementary material available at stacks.iop.org/njp/17/045003/mmedia.}

Figure 9. (a) Histogram of the ratio of the absorption signals for the $Q_1(1'') = 1.5$ resonant lines in SrOH exciting the diagonal $\tilde{A}^2\Pi_{\frac{1}{2}} (000) \rightarrow \tilde{X}^2\Sigma^+ (000)$ and off-diagonal $\tilde{A}^2\Pi_{\frac{1}{2}} (100) \rightarrow \tilde{X}^2\Sigma^+ (000)$ electronic transitions. We observe an average value of 5.2% with a standard deviation of 0.2%. Figure (b) shows the corresponding absorption signals as a function of time. To determine the histogram of the measured ratios, only the signal between 0.5 and 10 ms is used in the analysis.
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