Carrier Localization Effects in InGaN/GaN Multiple-Quantum-Wells LED Nanowires: Luminescence Quantum Efficiency Improvement and “Negative” Thermal Activation Energy

Wei Bao1,*,†, Zhicheng Su1,*, Changcheng Zheng1,2, Jiqiang Ning1,3 & Shijie Xu1

Two-dimensional InGaN/GaN multiple-quantum-wells (MQW) LED structure was nanotextured into quasi-one-dimensional nanowires (NWs) with different average diameters with a combination approach of Ni nanoislands as mask + dry etching. Such nanotexturing bring out several appealing effects including deeper localization of carriers and significant improvement in quantum efficiency (e.g., from 4.76% of the planar MQW structure to 12.5% of the 160 nm MQW NWs) of light emission in the whole interested temperature range from 4 K to 300 K. With the aid of localized-state ensemble (LSE) luminescence model, the photoluminescence spectra of the samples are quantitatively interpreted in the entire temperature range. In terms of distinctive temperature dependence of photoluminescence from these samples, a concept of “negative” thermal activation energy is tentatively proposed for the MQW NWs samples. These findings could lead to a deeper insight into the physical nature of localization and luminescence mechanism of excitons in InGaN/GaN nanowires.

It has been known for a long time that carrier localization is a ubiquitous phenomenon in real solid-state materials due to lattice disorder, impurities, and various imperfections including defects and deep centers, and thereby has a profound impact on both the electrical and optical properties of materials1. For example, the localized energy states caused by In composition fluctuations and In-rich nanostructures in InGaN alloy working as the active layer of efficient blue light-emitting diodes (LEDs) are closely related to the high efficiency of this kind of LEDs which is the key element in solid-state lighting technique revolution2,3. Usually, InGaN/GaN planar multiple-quantum-wells (MQW) structure acts as the active layer (light emitting layer) in the InGaN-based blue LEDs. To date, luminescence efficiency of InGaN/GaN MQW LEDs is still insufficient to support such a lighting technique revolution4. Moreover, efficiency droop problem in the operation of the blue LEDs under large injection current is a severe hinder5,6. Very recently, InGaN/GaN MQW nanorods or nanowires (NWs) have been proposed and explored as the active layer in order to achieve higher luminescence efficiency1–12. Some encouraging results, e.g., enhanced light extraction efficiency due to creation of the interspaceal regions between the wires and improved luminescence internal quantum efficiency due to suppression of the quantum confined Stark effect (QCSE) by partial relaxation of the lattice mismatch strain, have been achieved in these available studies. Even reduced exciton-phonon (e.g., longitudinal optical mode) coupling has been claimed by Renwick et al. in the post-growth nanotextured InGaN/GaN MQW nanorods13.

1Department of Physics, Shenzhen Institute of Research and Innovation (SIRI), and HKU-CAS Joint Laboratory on New Materials, The University of Hong Kong, Pokfulam Road, Hong Kong, China. 2Mathematics and Physics Centre, Department of Mathematical Sciences, Xi’an Jiaotong-Liverpool University, Suzhou 215123, China. 3Suzhou Institute of Nano-tech and Nano-bionics, Chinese Academy of Sciences, Suzhou 215123, China. †Present address: Department of Physics, University of Michigan, Ann Arbor, USA. *These authors contributed equally to this work. Correspondence and requests for materials should be addressed to S.J.X. (email: sjxu@hku.hk)
On the other hand, nanotexturing InGaN/GaN MQW planar structure into nanowires may bring out some other fascinating properties and phenomena such as new surface electronic states, new surface vibrational modes etc. Nevertheless, an in-depth investigation on localization, luminescence efficiency and mechanism of carriers in InGaN/GaN MQW nanowires is still lacking and highly desirable in terms of both fundamental and technological interests. In the present article this is done. We first examine the variable-temperature photoluminescence (PL) of InGaN/GaN MQW LED structure before and after the nanotexturing, and then make theoretical quantitative analysis to the experimental data with localized-state ensemble (LSE) luminescence model. Good agreement between theory and experiment enables us have a deeper insight into the physical nature of luminescence mechanisms in the InGaN/GaN MQW nanowires. We also propose a concept of “negative” thermal activation energy for describing anomalous temperature behaviors of luminescence of the InGaN/GaN MQW nanowires. These state-of-the-art findings and arguments could be commonly valid for very different materials with carrier localization.

From the top-view ((a) and (c)) and the tilted-view ((b) and (e)) SEM images of the two NWs samples in Fig. 1, it can be seen that the NWs are about 160 nm ((a) and (b)) and 100 nm ((c) and (d)) in diameter on average, respectively, and both are about 700 nm in height. Nanowire sheet densities of the 160 nm and 100 nm NWs samples are estimated to be $1.1 \times 10^7$ and $2.6 \times 10^7$ cm$^{-2}$, respectively. Figure 2 shows the micro-Raman spectra of the three samples at room temperature. Compared with the as-grown planar MQW sample, the two NWs samples exhibit an additional Raman scattering peak located at the lower energy side of the longitudinal optical (LO) phonon ($A_\text{g}$-LO, $736.23 \text{ cm}^{-1} \approx 91.3 \text{ meV}$) mode. Moreover, frequency dependence of this additional Raman mode on the nanowire size such as diameter distinctively follows the theoretical prediction on the surface optical phonon mode localized on the surface of nanoscale crystals. The appearance of the surface optical phonon mode indicates that the post-growth nanotexturing can alter significantly the optical properties of InGaN/GaN planar MQW structure. As addressed earlier, localization and luminescence mechanism of excitons in the nanotextured InGaN/GaN MQW structures are the central issue of the present study. Following discussion and arguments will concentrate on this issue.

Figure 3 illustrates the 3.6 K PL spectra of the as-grown planar MQW sample (solid line), 100 nm (solid line + solid circles) and 160 nm (solid line + open circles) NWs samples. The inset figure shows the close up view (semi-logarithmic scale) of the PL spectra near the band-edge transitions of GaN. After the nanotexturing, both significant effects, namely noticeable blue-shift in PL peak position and large enhancement in intensity, are observed. The blue-shift in PL peak position has been referred to as the largely reduced QCSE effect due to the obvious reduction of the original strong piezoelectric field by partial release of the lattice mismatch strain in the quantum wells. As for the significant enhancement in PL intensity, there are two possible reasons: (1) increase of the internal quantum efficiency (IQE) of luminescence due to the increased oscillator strength
caused by the band profile flattening; and (2) enhancement of the external light extraction efficiency due to the open volumes among the nanowires. In addition to the peak blue-shift and emission intensity increase, amazing transition of the PL lineshape from the broad multiple peaks before the nanotexturing to the almost single peak after the nanotexturing could be a more interesting phenomenon, which has not yet addressed in the literature. In our opinion, it may suggest a remarkable change in the localization and luminescence mechanism of carriers after the nanotexturing. As shown below, by examining temperature-dependent PL spectra of these samples, we may obtain a deeper insight into the carrier localization and luminescence mechanism in the samples, in particular in the two NWs samples.

To save space, we just depict the 3.6 K (Fig. 3) and 300 K PL spectra (Fig. 4) of the as-grown planar MQW sample (solid line) and the two NWs samples (solid lines + symbols). Compared with the 3.6 K PL spectra, the 300 K PL spectra of all the three samples broaden significantly. We now extract all the three chief spectral parameters, namely peak position (spectral center), integrated intensity and linewidth, from the measured variable-temperature PL spectra of the three samples. The obtained data are depicted in various solid symbols in Figs 5, 6 and 7 for the three samples. For the planar sample, we use a single Gaussian lineshape function to do a best fit to the measured PL spectra for getting the chief spectral parameters. As seen in Figs 6 and 7, S-shaped temperature dependence of the PL peak positions is observed for the two NWs samples, which is a typical temperature behavior of collective luminescence of localized excitons. Taking into account generation, thermal activation (e.g., non-radiative recombination, radiative recombination, and re-capturing of excitons, as well as assuming a Gaussian-type density of states for localized-state ensemble, a generalized luminescence model for localized-state ensemble (LSE) was developed by Li and Xu et al. According to this model, temperature-dependent PL peak positions can be written as

\[
A_{\text{LO}} = \frac{E_{\text{high}} - E_{\text{low}}}{1 - e^{-\frac{T}{T_0}}} + E_{\text{low}}
\]

Figure 2. Micro-Raman spectra of the three samples measured at room temperature and under the back-scattering geometric configuration. New surface optical phonon mode (denoted as SO) can be clearly observed for the NWs sample.

Figure 3. 3.6 K PL spectra of the three samples measured under the same conditions. The inset shows close-up spectra near the band-edge emission of GaN. Compared with the planar MQW sample, both NWs samples show significantly improved emission intensity at low temperatures, especially the 160 nm NWs sample.
Figure 4. **Room-temperature PL spectra of the three samples.** Again, the NWs samples exhibit improved emission intensity at room temperature. In particular, the 160 nm NWs sample shows a substantial improvement in PL intensity.

Figure 5. **Extracted peak positions, FWHM and integrated intensities of the planar MQW sample at different temperatures.** The solid lines are the fitting curves with LSE model.

\[ E(T) = E_0 - \frac{\alpha T^2}{T + \Theta} - \beta(T) \cdot k_b T, \]  

(1)

where \( \beta(T) \) is a temperature-dependent dimensionless parameter which can be obtained by numerically solving the following equation:
Figure 6. Extracted peak positions, FWHM and integrated intensities of the 160 nm NWs sample at different temperatures. The solid lines are the fitting curves with LSE model.

Figure 7. Extracted peak positions, FWHM and integrated intensities of the 100 nm NWs sample at different temperatures. The solid lines are the fitting curves with LSE model.
Δ as the QCSE weakening effect largely due to the strain relaxation induced by nanotexturing 7–10,13. However, for the resulting 100 nm NWs, planar structure was nanotextured into 160 nm nanowires, however, the luminescence linewidth. This is the main reason why the PL peak of the planar sample doesn’t show obvious the variable-temperature PL measurements on both the NWs samples under the different excitation intensities. 

Energy in terms of their abnormal temperature dependence of luminescence peak and positive Δ quenching of luminescence in InGaN/GaN nanowires may be characterized by “negative” thermal activation Δ such cases, Δ states (or sites in real space) with higher energies, as schematically shown as dashed horizontal line in Fig. 8. In the figure, the wavy arrows stand for the thermal activation processes, Δ ns rise and the absolute value of Δ can take positive (±) or negative (−) signs. For the InGaN/GaN material systems investigated in the present work, Δ usually takes a positive sign18,19. Actually, if luminescence quantum efficiency η is defined as η = , Eq. (2) can be re-written as

By using Eqs (1) and (3), we may get several chief parameters characterizing luminescence of localized excitons via making a best fit to the temperature dependence of PL peak position. Parameters adopted in the fitting are tabulated in Table 1. A unified Debye temperature Θ = 630 K is taken in the fitting for all the three samples. As mentioned earlier, noticeable blue-shift in peak position and large increase in emission intensity are the two significant effects observed after the nanotexturing. For example, it increases from 2.7850 eV of the planar MQW structure to 2.8065 eV of the 160 nm NWs sample, further to 2.8472 eV of the 100 nm QWs sample. This phenomenon has been well documented and interpreted as the QCSE weakening effect largely due to the strain relaxation induced by nanotexturing7–10,13. However, for the luminescence intensity increase after the nanotexturing, its origin has not yet well understood. In the present study, the luminescence quantum efficiency is obtained for the three samples. From Table 1, the luminescence quantum efficiency of the two NWs samples is much higher than that of the planar MQW sample. In particular, the luminescence efficiency of the 160 nm NWs sample is about 2.6 times stronger than that of the planar sample. Such result is very encouraging because enhancement of the luminescence quantum efficiency is our central objective. But, when the nanowires’ average diameter is reduced to about 100 nm, the luminescence quantum efficiency drops, i.e., from 12.5% of the 160 nm NWs to 7.69% of 100 nm NWs. This efficiency decrease could be attributed to the enhanced surface state effect leading to nonradiative recombination in small size nanowires.

It has been known for a long time that the S-shaped temperature dependence of the PL peak position is a characteristic behavior of localized carriers in semiconductors. By using the LSE luminescence model, the S-shaped temperature dependence of the PL peak positions of both the 160 nm and 100 nm NWs samples can be well reproduced, as shown in Figs 6 and 7. As argued earlier, ΔE = Ea − E0 rather than E0 itself plays a more significant role in determining abnormal temperature dependence of luminescence of localized carriers. For the as-grown planar MQW LED structure, its ΔE = 11.2 meV is much smaller than parameter ΔE = 19.80 meV and the luminescence linewidth. This is the main reason why the PL peak of the planar sample doesn’t show obvious S-shaped temperature dependence. Instead of, the peak positions show a “chair”-shaped temperature dependence due to large parameter ΔE (characterizing the distribution width of localized states), as seen in Fig. 5. After the planar structure was nanotextured into 160 nm nanowires, however, ΔE significantly increases to 14.3 meV. For the resulting 100 nm NWs, ΔE further increases to 27.2 meV. It should be noted that in general cases, ΔE may take negative sign7. That implies that E0 is usually above E0 in which localized carriers are thermally activated to states (or sites in real space) with higher energies, as schematically shown as dashed horizontal line in Fig. 8. In such cases, ΔE takes a negative value, but is usually assigned as “positive” thermal activation energy. However, in the InGaN/GaN system, especially in their nanowires, ΔE takes a positive value. We thus argue that the thermal quenching of luminescence in InGaN/GaN nanowires may be characterized by “negative” thermal activation energy in terms of their abnormal temperature dependence of luminescence peak and positive ΔE. In Fig. 8, we schematically illustrate such cases, e.g., E0 below E0, then ΔE = E0 − E0 takes a positive value, but defined as a “negative” thermal activation energy. In the figure, the wavy arrows stand for the thermal activation processes, while the straight downward arrow represents luminescence transition. The bottom curve represents a luminescence spectrum of localized-state ensemble. For the studied NWs samples, as argued earlier, strongly reduced QCSE effect takes place due to the strain relaxation and hence piezoelectric electric field reduction. As a result, E0 could rise and the absolute value of ΔE might increase. Indeed, our experimental results demonstrate this tendency. In order to further verify the occurrence of largely reduced QCSE effect in the NWs samples, we conducted the variable-temperature PL measurements on both the NWs samples under the different excitation intensities.

| Sample          | σ (meV) | E0 (eV) | ΔE (meV) | η  | γ  | α (meV/K) |
|-----------------|---------|---------|----------|----|---|-----------|
| 160 nm NWs      | 11.10   | 2.8065  | 14.3     | 12.5% | 0.21 | 0.451     |
| 100 nm NWs      | 16.30   | 2.8472  | 27.2     | 7.69% | 0.36 | 0.643     |
| Planar MQW      | 19.80   | 2.7850  | 11.2     | 4.76% | 0.34 | 0.245     |

Table 1. Parameters for the three samples.
Shown in Fig. 9 are the peak positions (symbols) of measured PL spectra of the 160 nm and 100 nm NWs samples against temperature for three different excitation powers. As expected, the PL peak shifts toward higher energy direction as the excitation intensity increases, especially at low-medium temperatures. Again, we employ Eqs (1) and (2) to make a fit to the experimental data, and good agreement between theory and experiment is achieved. The solid lines represent the fitting curves.

In addition to the peak position, full width at half maximum height (FWHM) or simply linewidth is another key parameter which also carries important information on localization mechanism of carriers. Reduction in linewidth with temperature in a temperature range is another PL signature of carrier localization principally due to the thermal redistribution of localized excitons among different localized states. According to the LSE model, the thermal distribution of localized excitons is jointly determined by Gaussian-type density of states and a newly-derived distribution function. In mathematic form, the thermal distribution of localized excitons can be described by

\[
n(E, T) = \rho(E) \cdot f(E, T).
\]

Here \( \rho(E) = \rho_0 \exp\left[-(E - E_0) / 2\sigma^2\right] \) is a standard Gaussian function and \( f(E, T) = \left[\exp\left((E - E_0)/k_BT\right) + \tau_{\nu\nu} / \tau_{\gamma}\right]^{-1} \) is a newly derived distribution function for localized carriers. It has been proven that \( n(E, T) \) essentially represents the spectral profile of localized-state ensemble luminescence. The FWHM \( \Gamma(T) \) of \( n(E, T) \) is thus obtained by numerically solving \( n(E, T) = n(E_{ph}, T)/2 \). Besides, phonon scattering induced broadening shall be taken into account. By doing so, we can write down the expression for the actual linewidth of localized-state ensemble luminescence:

\[
\Gamma = \Gamma_0 + \Gamma_c(T) + \sigma_{\Delta}T + \frac{\gamma_{LO}}{e^{\hbar_{LO}/k_BT} - 1},
\]

(4)

Figure 8. A physical picture showing the luminescence mechanism of localized-state ensemble. Several key energy parameters are denoted, especially \( +\Delta E \) and \( -\Delta E \) which represent positive and negative thermal activation energy, respectively, corresponding to the normal thermal quenching and abnormal thermal quenching of luminescence.

Figure 9. Peak positions (symbols) of the measured PL spectra vs. temperature for the 160 nm NWs and 100 nm NWs samples for three different excitation powers. The solid lines are the fitting curves with LSE model.
The starting sample used in this study was a typical MQW LED structure consisting of layers in the order from top to bottom: a 0.2 μm p-type GaN:Mg top layer, then 5 periods of InGaN/GaN MQWs with barrier’s (well’s) thickness of 30 nm (3 nm), and a 3.0 μm n-type GaN:Si buffer bottom layer, which was grown on c-plane sapphire with metalorganic chemical vapor deposition. The nanowires were prepared with the “top-down” dry etching process using Ni self-assembled nanoislands as the etching mask. Other preparation details of the NWs can be referred to a publication24.

A JEOL (JSM-7001F) SEM microscopy was employed to characterize the dimensions of the nanopillars. Micro-Raman scattering spectra were measured on an integrated W Tec Alpha scanning confocal micro-Raman system with the back-scattering geometric configuration14. In the Raman scattering measurements, the 514.5 nm line of an argon ion gas laser was used as the excitation source. Variable-temperature PL spectral measurements were carried out on a home-made PL system using a Kimmon 325 nm He-Cd laser as the excitation light source. The maximum output power of the He-Cd laser was 38 mW. In the PL measurements, the samples were mounted on the cold figure of a Janis closed cycle cryostat proving a varying temperature range of 3.6–300 K. A detailed description of the PL setup can be referred to a previous publication25.
References

1. Anderson, P. W. Absence of diffusion in certain random lattices. Phys. Rev. 109, 1492–1505 (1958).
2. Nakamura, S. The roles of structural imperfections in InGaN-based blue light-emitting diodes and laser diodes. Science 281, 956–961 (1998).
3. O’Donnell, K., Martin, R. & Middleton, P. Origin of luminescence from InGaN diodes. Phys. Rev. Lett. 82, 237–240 (1999).
4. See, for example, a recent review, Pimpukar, S., Speck, J. S., DenBaars, S. P. & Nakamura, S. Prospects for LED lighting. Nat. Photon 3, 180–182 (2009).
5. Ireland, J., Martinelli, L., Peretti, J., Speck, J. S. & Weisbuch, C. Direct measurement of Auger electrons emitted from a semiconductor light-emitting diode under electrical injection: identification of the dominant mechanism for efficiency droop. Phys. Rev. Lett. 110, 177406 (2013).
6. Sarkissian, R., Roberts, S. T., Yeh, T-W., Das, S., Bradforth, S. E., O’Brien, J. & Dakkus, P. D. Photon quenching in InGaN quantum well light emitting devices. Appl. Phys. Lett. 103, 041123 (2013).
7. Li, S. F. & Waag, A. GaN based nanorods for solid state lighting. J. Appl. Phys. 111, 071101 (2012).
8. Kawakami, Y. et al. Optical properties of InGaN/GaN nanopillars fabricated by postgrowth chemically assisted ion beam etching. J. Appl. Phys. 107, 023522 (2010).
9. Chen, L.-Y. et al. High performance InGaN/GaN nanorod light emitting diode arrays fabricated by nanosphere lithography and chemical mechanical polishing processes. Opt. Express 18, 7664–7669 (2010).
10. Zhu, J. H. et al. Light extraction efficiency improvement and strain relaxation in InGaN/GaN multiple quantum well nanopillars. J. Appl. Phys. 109, 084339 (2011).
11. Bai, J., Wang, Q. & Wang, T. Characterization of InGaN-based nanorod light emitting diodes with different indium compositions. J. Appl. Phys. 111, 111013 (2012).
12. Dong, P. et al. Optical properties of nanopillar AlGaN/GaN MQWs for ultraviolet light-emitting diodes. Opt. Express 22, A320–A327 (2014).
13. Renwick, P., Tang, H., Bai, J. & Wang, T. Reduced longitudinal optical phonon-exciton interaction in InGaN/GaN nanorod structures. Appl. Phys. Lett. 100, 182105 (2012).
14. Zhu, J. H. et al. Localized surface optical phonon mode in the InGaN/GaN multiple-quantum-wells nanopillars: Raman spectrum and imaging. Appl. Phys. Lett. 99, 113115 (2011).
15. Wang, X. H., Ning, J. Q., Xu, S. J. & Choi, H. W. Raman and photoluminescence characterization of focused ion beam patterned InGaN/GaN multi-quantum-wells nanopillars array. J. Appl. Phys. 110, 093111 (2011).
16. Ruppern, R. & Englman, R. Optical phonons of small crystals. Rep. Prog. Phys. 33, 149–196 (1970).
17. Sernelius, B. E. Surface Modes in Physics. John Wiley & Sons (2011).
18. Li, Q. et al. Thermal redistribution of localized excitons and its effect on the luminescence band in InGaN ternary alloys. Appl. Phys. Lett. 79, 1810–1812 (2001).
19. Li, Q., Xu, S. J., Xie, M. H. & Tong, S. Y. Origin of the ‘S’-shaped temperature dependence of luminescent peaks from semiconductors. J. Phys.: Condens. Matter 17, 4853–4858 (2005).
20. Li, Q., Xu, S. J., Xie, M. H. & Tong, S. Y. A model for steady-state luminescence of localized-state ensemble. Europhys. Lett. 71, 994–1000 (2005).
21. Rudin, S., Reinecke, T. & Segall, B. Temperature-dependent exciton linewidths in semiconductors. Phys. Rev. B 42, 11218–11231 (1990).
22. Xu, S. J. et al. Comparative study on the broadening of exciton luminescence linewidth due to phonon in zinc-blende and wurtzite GaN epilayers. Appl. Phys. Lett. 81, 4389–4391 (2002).
23. Chen, D. et al. Enhancement of electron-longitudinal optical phonon coupling in highly strained InGaN/GaN quantum well structures. J. Appl. Phys. 101, 053712 (2007).
24. Zhu, J. H. et al. Fabrication and optical characterization of GaN-based nanopillar light emitting diodes. Chin. Phys. Lett. 25, 3485–3488 (2008).
25. Xu, S. J., Liu, W. Li, M. Effect of temperature on longitudinal optical phonon-assisted exciton luminescence in heteroepitaxial GaN layer. Appl. Phys. Lett. 77, 3376–3378 (2000).

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Author Contributions

W.B. performed the Raman and PL measurements, as well as preliminary data processing. Z.C.S. did theoretical fittings with LSE model. S.J.X. contributed the main ideas, including the concept of "negative" thermal activation energy, for the quantitative interpretation of the data and phenomenon and supervised the project. W.B. drafted the first version of manuscript and S.J.X. completed and finalized the manuscript. C.C.Z. and J.Q.N. participated in the Raman and PL measurements and data analysis and discussion.

Additional Information

Competing financial interests: The authors declare no competing financial interests.

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