Galaxy properties from voids to clusters in the SDSS-DR4

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ABSTRACT

Aims. We investigate the environmental dependence of galaxy population properties in a complete volume-limited sample of 91566 galaxies in the redshift range 0.05 ≤ z ≤ 0.095 and with M_r ≤ −20.0 (that is M^* + 1.45), selected from the Sloan Digital Sky Survey (SDSS) Data Release 4 (DR4). Our aim is to search for systematic variations in the properties of galaxies with the local galaxy density. In particular, we analyze how the (u − r) color index and the morphological type of galaxies (the latter evaluated through the SDSS Eclass and fracDev parameters) are related to the environment and to the luminosity of galaxies, in order to find hints that can be related to the presence of a "void" galaxy population.

Methods. "Void" galaxies are identified through a highly selective criterion, which takes also into account redshift and allows us to exclude from the sample all the galaxies that are not really close to the center of underdense regions. We study the (u − r) color distribution for galaxies in different luminosity bins, and we look for correlations of color with the environment, the luminosity, and the morphological type of the galaxies.

Results. We find that galaxies in underdense regions (voids) have lower luminosity (M_r > −21) and are bluer than cluster galaxies. The transition from overdense to underdense environments is smooth, the fraction of late-type galaxies decreases while the fraction of early-type galaxies increases smoothly from underdense to dense environments.

Conclusions. We do not find any sudden transition in the galaxy properties with density, which, according to a suggestion by Peebles (2001), should mark the transition to a population of "void" galaxies in CDM models. On the contrary, our results suggest a continuity of galaxy properties, from voids to clusters.

Key words. Large-scale structure of Universe – Galaxies: fundamental parameters (classification, colors, luminosities) – Galaxies: statistics

1. Introduction

A self-consistent theory of galaxy formation and evolution within the gravitational collapse paradigm has yet to come, although quite significant advancements have been recently done (e.g. Silk (2004) for an up-to-date review). Such a theory should explain the observed properties of galaxy populations in different environments, ranging from very dense clusters to large voids. However, the mere existence of galaxies within voids is a challenge for any gravitational bottom-up scenario of the Large Scale Structure (LSS) formation in the Universe, because in this scenario voids form out of the expansion of underdense (δ < 0) initial density fluctuations. Theoretical models and numerical simulations (e.g. Olson & Silk 1975, Bolejko et al. 2005) suggest that dark matter flows out of voids, and partly concentrates in some thin boundary shells. The latter, however, have not been detected, although there is clear evidence that the galaxy density profiles inside voids become steeper near their borders (Lindner et al. 1996, Hoyle & Vogeley 2004, Goldberg et al. 2005). Observationally, there is evidence that voids are surrounded by superclusters of galaxies, as is vividly shown by recent analyses of the Las Campanas and SDSS surveys (Einasto et al. 2003, R. 2005). It is interesting to note that the void models of Olson & Silk (1975) and Hoyle et al. (2005) are only concerned with the global dynamics of dark matter (DM): much less work has been devoted to understand the non-linear collapse of DM halos and the formation of galaxies within voids. Dekel & Silk (1986) suggested that voids could be populated by a population of faint dwarf galaxies, where star formation is suppressed by strong photoionization occurred at z > 6 (Hoeft et al. 2005).

The search for galaxies in voids started with the discovery of the voids themselves (i.e. Lindner et al. 1996 for a full review in this field until 1996), Popescu et al. (1996, 1997) looked for emission-line galaxies in nearby voids, concluding that most of them are found close to the borders, and far from the deep internal regions. There have also been (failed) attempts at detecting a population of dwarf galaxies more homogeneously distributed within voids (Sabatini et al. 2003, 2005; Roberts et al. 2004), but the lack of an evident faint end of the dwarf galaxies luminosity function does not allow to make firm quantitative predictions about their abundance.

Since the seminal papers by Grogin & Geller (1999, 2000), some efforts have been dedicated to detect and to study the properties of bright galaxies in nearby voids. The availability of large samples of galaxies from surveys like the 2dF and the Sloan Digital Sky Survey (SDSS) has made possible more complete analysis of the dependence of galaxy properties on the environment. Croton et al. (2005) have shown that the luminosity function in voids tends to have a steeper slope at high luminosity, but not in the fainter range. The dependence of (u − r) color distribution on the environment has also been recently studied by Balogh et al. (2004), who found that its shape is bimodal and can be well described by a linear combination of two gaussian distributions for
a very wide range of local densities. Surprisingly, they also find a small quantity of red, early-type galaxies even in the lowest density environments, thus suggesting that there is not a rigid morphological or color segregation with environment. However, the environmental dependence of galaxy properties is only detected for galaxies in the luminosity range \( -20.4 < M_r < -19.4 \) (Tanaka et al., 2004): for galaxies brighter than \( M_r = -20.4 \) there are very little variations of their properties with the environment. Peebles (2001) suggested that galaxies lying within very underdense regions are representative of a distinct population. In this case, we should observe a transition in one or more galaxy properties moving from clusters to voids.

To verify the previous hypothesis, we will investigate the variation of the color distribution, morphology, and luminosity with the local density. This kind of analysis has been made possible by the availability of a large sample of galaxies extracted from the SDSS - Data Release 4 (SDSS-DR4: York et al., 2000; Stoughton et al., 2002; Abazajian et al., 2004). Using this huge data sample we confirm some previous results (e.g., Rojas et al., 2002; Abazajian et al., 2004). Using this huge data sample we confirm some previous results (e.g., Rojas et al., 2003), and we are able to extract statistically significant subsamples for different relative underdensities. We will study the correlation between \((u-r)\) colors and the environment for bright and faint galaxies, also looking for sudden changes which should mark the emergence of a distinct void galaxy populations, as suggested by Peebles (2001). We will use a criterion to estimate the density which is different from the \(\Sigma_r\) criterion used by, e.g., Tanaka et al. (2004): on the contrary, it is more similar to the one adopted by Rojas et al. (2004), because we want to be sure that galaxies in voids are correctly identified and included in the sample.

The plan of the paper is as follows: after the description of the galaxy sample (sect. 2), in section 3 we will discuss the adopted criteria to construct our subsamples. In section 4 we will present our results concerning the \((u-r)\) color distribution, and its dependence on the local density and luminosity. In section 5 we will analyze the results of the previous section taking also into account the relationship between the \((u-r)\) color distribution and the morphological type of galaxies, then discussing the relationship with the morphology-density relation (Dressler 1980). Finally, in section 6 and in section 7 we will present a general discussion and our conclusions.

Throughout, we adopt standard present day values of the cosmological parameters to compute comoving distances from redshift: a density parameter \(\Omega_m = 0.3\), a cosmological constant \(\Omega_{\Lambda} = 0.7\), and a Hubble’s constant value \(H_0 = 75\) km s\(^{-1}\) Mpc\(^{-1}\).

2. SDSS - DR4

The SDSS (York et al., 2000; Abazajian et al., 2004; 2005; Adelman-McCarthy 2005) is a photometric and spectroscopic survey, which will map about one quarter of the entire sky outside the Galactic plane, and will collect spectra of about \(10^6\) galaxies, \(10^5\) quasars, 30,000 stars and 30,000 serendipity targets.

Photometry is available in \(u'\), \(g'\), \(r'\), \(i'\) and \(z'\) bands (Fukugita et al., 1996; Gunn et al., 1998), while the spectroscopic data are obtained with a pair of multi-fiber spectrographs. Each fiber has a diameter of 0.2 mm (3" on the sky), and adjacent fibers cannot be located more closely than 55" on the sky (\(-110\) kpc at \(z = 0.1\) with \(H_0 = 75\) km s\(^{-1}\) Mpc\(^{-1}\)) during the same observation. In order to optimize the placement of fibers on individual plates, and as the placement of plates relative to each other, a tiling method has been developed which allows a sampling rate of more than 92% for all targets. For details see the SDSS web site (www.sdss.org/dr4/algorithms/tiling.html).

The spectroscopic SDSS-DR4 catalog contains about 673,280 galaxies and covers an area of 4783 square degrees. The spectra cover the spectral range \(3800 < \lambda < 9200\) Å, with a resolution of \(1800 < \lambda/\Delta\lambda < 2100\), and give a rms redshift accuracy of 30 km s\(^{-1}\), to an apparent magnitude limit of Petrosian magnitude of \(r' = 17.77\).

Data have been obtained from the SDSS database (http://www.sdss.org/DR4), using the CasJobs facility (http://casjobs.sdss.org/casjobs/).

3. Sample selection

In this paper, we will take into account a complete volume-limited sample of galaxies in the redshift range \(0.05 \leq z \leq 0.095\), brighter than \(M_r = -20.0\), that is \(M_r^* = 1.45\), with \(M_r^* = -21.45\). The lower redshift limit is chosen with the aim of minimizing the aperture bias (e.g., Gómez et al., 2003) caused by the presence of large nearby galaxies, while the upper limit is aimed at obtaining a high level of completeness, estimated through Schmidt’s \(V/V_{\text{max}}\) test.

Our initial sample contains 91566 galaxies. For each galaxy, we compute its r-band absolute magnitude, dereddened and K-corrected as suggested in Blanton et al. (2003). The distributions of \(z\) and \(M_r\) are given in Fig. 1.

Galaxies in our sample with no detectable emission lines in their spectra are classified as Passive Galaxies (PGs); for these galaxies, the morphological type should be earlier than Sa. Galaxies with one or more emission lines having \(I_1/\sigma_{I_1} > 2\), where \(I_1\) is the emission line flux and \(\sigma_{I_1}\) its uncertainty, are classified as star forming galaxies (SFGs), according to the criteria adopted by Kewley et al. (2001): for these galaxies, the morphological type should be later than S0/Sa. In order to avoid all the ambiguous cases in the AGN/SFG classification, we removed those
sources whose line ratios fall close to the border line of the diagnostic diagrams. This was done by keeping only those sources for which part of the error bar associated to the logarithm of the line-ratios lie within the theoretical uncertainty of the model ($\sigma_{\text{mod}} = 0.1$ dex) in both $x$ and $y$ directions.

Moreover, we adopted another criterion to separate the galaxies in early- and late-type, according to their morphological type defined by the two parameters $e\text{class}$ and $\text{fracDev}$ provided by the SDSS. $\text{fracDev}$ is a photometric parameter providing the weight of a de Vaucouleurs component in best composite exponential+de Vaucouleurs models, and $e\text{class}$ is a spectroscopic parameter giving the spectral type from a principal component analysis. Early-type galaxies (E+S0) were selected following the criteria adopted by Bernardi et al. (2005): $\text{fracDev}(r) > 0.8$ and $e\text{class} < 0$. Late-type galaxies (Sa and later) were selected when either $e\text{class} \geq 0$ or $\text{fracDev}(r) < 0.5$. In this way we exclude from our analysis all the galaxies for which an unambiguous classification is not possible, because their $e\text{class}$ and $\text{fracDev}$ parameters are out of the previous defined ranges.

In order to investigate a possible dependence of galaxy colors on the environment, for each galaxy we compute the number of neighbours within a fixed radius $D_{\text{max}} = 5$ Mpc, the distribution and the related percentile (Tab. 1). We adopted this particular distance because it was used in previous works aimed at studying galaxies in very underdense regions (voids) (Grogin & Geller, 1999; Hovle & Vogelsberger, 2004). The use of the percentile in our analysis allows us to compare different environments and to characterize the difference between over- and underdense regions without defining an environment a priori.

A galaxy $j$ is considered as a neighbour of a galaxy $i$ if:

- $D_{ij} \leq D_{\text{max}}$
- $|c(z_i) - z_j| \leq 1000$ km s$^{-1}$

where $D_{ij}$ is the projected distance between the two galaxies, and $|c(z_i) - z_j|$ is their redshift difference. $D_{ij}$ is computed from the angular separation $\theta_{ij}$ and the redshift $z_i$; the limit $|c(z_i) - z_j| \leq 1000$ km s$^{-1}$ is the value usually adopted to select cluster or galaxy group members in the velocity space (Fadda et al., 1996; Wilman et al., 2005). Throughout, we intend as local galaxy density the number of neighbours brighter than $M_r = -20.00$ and within 5 Mpc.

In Appendix A we explore the effect of varying our definition of local galaxy density on scales 2.5 Mpc to 10 Mpc. We find that our conclusions remain unchanged.

Table 1. Numbers of neighbours and the related percentile. A percentile is defined as the value of a given scalar quantity characterizing the fraction of the distribution that is equal or smaller than that value.

| $N_{\text{neigh}}$ | Percentile |
|------------------|-----------|
| 0                | 1st       |
| 2                | 5th       |
| 4                | 10th      |
| 9                | 25th      |
| 18               | 50th      |
| 35               | 75th      |
| 59               | 90th      |
| 79               | 95th      |
| 127              | 99th      |

4. ($u - r$) color distribution: dependence on environment and luminosity

It is well known that the environment can affect the colors of galaxies, and that galaxies in low density environment are generally bluer than galaxies in clusters (Grogin & Geller, 1999). However, we cannot relate the color of galaxies to their environment because the ($u - r$) color does not correlate with the local density in a single way. Then, because the luminosity function of bright galaxies decreases steeply with increasing luminosity, we investigated whether the differences between cluster and void galaxies are also a function of their luminosity, as suggested by Rojas et al. (2004). In Fig. 2 we analyze the ($u - r$) color distribution for all the galaxies in our sample (left panel), for galaxies in different environments (central panel), and for two different ranges of luminosity (right panel). To this last aim, we adopted the median value of the luminosity distribution to define two different ranges of luminosities: $M_r$ fainter and brighter than $M_r = -20.7$.

Galaxies in underdense environments (defined as those having $N < 4$ neighbours within 5 Mpc, where $N = 4$ corresponds to the 10th percentile) and galaxies fainter than $M_r = -20.7$ have a similar, bimodal, color distribution. The second peak is redder and coinciding with the peak of the color distribution for galaxies in dense environments ($N > 59$ neighbours, corresponding to the 90th percentile) and brighter than $M_r = -20.7$. From this first analysis, it is evident that, in general, galaxies in underdense environments are bluer and fainter than galaxies in dense environments.

In Fig. 3 differences between over- and underdense regions, as characterized by the number of neighbours, are increasing from left to right. For instance, in the rightmost panels, the distributions are referred to galaxies having more than 127 or less than 1 neighbours within 5 Mpc, corresponding to the 1st and 99th percentiles of the global distribution, respectively. In this way we are able to compare environments that are more and more extreme. These plots confirm that in underdense regions galaxies tend to be bluer than cluster galaxies, and the transition from over- to under-dense regions is smooth. In Fig. 5 the galaxy populations for different environment are compared, using progressively fainter galaxies, from left to right. Galaxies in underdense environment ($N_{\text{neigh}} \leq 25$th or $N_{\text{neigh}} \leq 5$th) are bluer at fainter luminosities and the transition is smooth: this result is confirmed by a KS test and it is also in accordance with Rojas et al. (2004).

Then, we conclude that both luminosity and density act to discriminate galaxies in underdense environments from galaxies in the field or in clusters.

In the following, we will make these statements more quantitative.

In order to quantify the difference between over- and underdense regions, we compute a median value of ($u - r$), defined as the difference of the median value ($u - r$) between the distributions of two opposite percentile. We define as opposite percentile the value 1-$p$, being $p$ the value of the percentile. For example, the 20$\text{th}$ percentile the opposite percentile is the 80$\text{th}$ so that, for this example, $\text{Median}_{20\text{th}}$ will be:

$$\text{Median}_{20\text{th}} = (u - r)_{N<20\text{th}} - (u - r)_{N>80\text{th}}$$

(1)

where ($u - r$) is the median value of the distribution. The plot in Fig. 4 shows a clear trend in the variation of the previous quantity with the color. It is interesting to observe that the variation is a smooth function of the difference in percentiles; we do not observe a very steep change of the slope for small values of the percentile, i.e., for very different environments. This result is a further hint at the fact that there is not a “void galaxy popula-
5. \((u - r)\) color distribution: dependence on morphology

In the previous section, we studied the dependence of the \((u - r)\) color distribution for the galaxies on both the environment and the luminosity, without to consider any dependence on their morphological type. But it is well known that the morphological type of galaxies correlates with density (Dressler, 1980) and color (Strateva et al., 2001), as well as there is also a correlation between density, luminosity and color (Hogg et al., 2003).

We also found that galaxies in underdense environments are bluer than galaxies in dense environment, in accordance with Baldry et al. (2004), but it is unclear if this is an induced effect driven by some other relation, e.g. the morphology-density relation (Dressler, 1980). Because the value \((u - r) = 2.22\) can be used to separate early- from late-type galaxies (Strateva et al., 2001) and because a clear bimodality is observed in the \((u - r)\) color distribution, in this section we will investigate the existence of a possible correlation between the findings in sect. 4 and the morphology. In particular, in order to relate the morphology to the environment, we compare the \((u - r)\) color distribution for early- and late-type galaxies with the color distribution of the total sample of galaxies.

From Fig. 6 we see that the bimodal shape of the \((u - r)\) color distribution.
1. **Fig. 3.** $(u-r)$ color distribution for galaxies in different environments.

2. **Fig. 4.** The trend of $\Delta$median, defined in the text, as a function of the percentile.

3. **Table 3.** Number of galaxies in the plots of Fig. 8

| Luminosity Range | Total (N) | Early (%) | Late (%) |
|------------------|-----------|-----------|----------|
| $M_r < -22$      | 361       | 75.3      | 1.5      |
| $-22 \leq M_r < -21$ | 27813     | 55.1      | 9.3      |
| $-21 \leq M_r \leq -20$ | 60134     | 36.0      | 29.8      |

The color distribution is a function of both the environment and the morphological type, becoming redder with increasing the density of the environments, as well as the fraction of early-type galaxies: in poor systems (i.e. $0 \leq N < 4$) the fractions of early- and late-type galaxies are similar; with increasing the number of neighbours the fraction of early-type galaxies also increases and the bimodality almost disappears (i.e. $59 \leq N < 127$). The numbers $N$ of galaxies used in Fig. 8 are not casual, but they rather correspond to the percentiles of the total distribution (Tab. 1).

In the previous section it has also been observed that the bimodal $(u-r)$ color distribution depends on both the environment and the luminosity. In fact, the fraction of blue galaxies decreases becoming more and more red with increasing of both the environmental density and the luminosity (Fig. 5), in accordance with Baldry et al. (2004) and Menci et al. (2005). Then in order to relate this result to the morphological type, we plot the $(u-r)$ color distribution for different ranges of luminosities and morphologies (Fig. 8). We find that the fraction of early-type galaxies decreases, while the fraction of late-type galaxies increases in samples which are over fainter, then
probing the environmental dependence on the luminosity of the ($u - r$) color distribution for early- and late-type galaxies.

Finally, we consider the ($u - r$) color distribution for galaxies having different morphological type and in different bins of magnitudes. Galaxies with $-21 \leq M_r < -20$ have a similar fraction of early (36.0%) and late (29.8%) type galaxies; for $-22 \leq M_r < -21$ these fractions are 55.1% (early) and 9.3% (late), while for $M_r < -22$ the fraction of late-type galaxies is negligible (1.5%) compared to the fraction of early-type (75.3%). In general, we have a similar trend (Fig. 8): the fraction of late-type galaxies decreases with increasing of both the environmental density and luminosity, while the fraction of early-type galaxies increases, then confirming the previous findings concerning the environmental dependence on the luminosity of the ($u - r$) color distribution for early- and late-type galaxies. Moreover, the color distributions for early-type/PGs and late-type/SFGs galaxies defined as described in sec. 3., are similar (Fig. 7), so that we can relate the environmental properties of late-type galaxies not only to the morphology-density relation (Dressler, 1980), but also to their star-forming activity.

6. Discussion

By definition, there are few galaxies in voids, and only the availability of large samples can allow to build statistically significant catalogues of galaxies in such underdense regions. These conditions are met by the sample we use in this paper, extracted from the SDSS-DR4.

Studying the galaxy properties in extremely underdense environments is an interesting test for cosmological and galaxy formation models. In standard CDM models, underdense regions should be populated with sub-$L^*$ galaxies (Dekel & Silk, 1986). Many of these “void dwarfs” were successfully identified in previous surveys. For example Lindner et al. (1995, 1996) found that their density decreases towards the center of the voids themselves. Recent surveys like the SDSS show the presence of both isolated galaxies and filaments thereof within voids (Einasto et al., 2003b), a circumstance which is also the result of numerical simulations (Antonuccio-Delogu et al., 2002; Gottlöber et al., 2003). Because these coherent structures are difficult to identify in galaxy surveys, recently many effort have been carried out to detect filaments (Pimbblet, 2005).

Peebles (2001) notices that the existence of a particular class of void-galaxies marked by a discontinuity in the observed properties of galaxy populations, from over- to underdense regions, would be a distinctive feature of galaxy formation in CDM mod-
els. On the contrary, our results (e.g., Figure 5) point out a smooth transition in colors and other properties with average density. This result is also confirmed when we consider the difference between truly void-galaxies and "wall" galaxies, then suggesting that does not exist a "pure" void-galaxy population, distinguished from the average galaxy population. However, the only study of galaxy colors as a function of the environment gives a partial view. In fact, the color of galaxies in underdense environments has a different distribution from that of galaxies in dense environment (red), as shown in Fig. 2. On the contrary, in underdense environments, the distribution of the galaxy populations without taking into account the morphological type is not equally skewed towards blue colors, confirming the findings by Balogh et al. (2004). Galaxies become bluer only if we consider a very underdense environment. When we consider galaxies fainter than $M_r = -22.0$, their color becomes more and more blue in environments that are more and more underdense ($N_{\text{neigh}} < 25^{th}$, $N_{\text{neigh}} < 10^{th}$, $N_{\text{neigh}} < 5^{th}$, $N_{\text{neigh}} < 1^{st}$). A similar trend (shifted to the red) is observed for galaxies in environments more and more dense ($N_{\text{neigh}} > 75^{th}$, $N_{\text{neigh}} > 90^{th}$, $N_{\text{neigh}} > 95^{th}$, $N_{\text{neigh}} > 99^{th}$), (Fig. 3). This trend becomes more and more evident when we consider galaxies more and more faint. We find that in dense environments, galaxies fainter than $M_r = -21$ are redder than galaxies in underdense environments (Fig. 5), confirming that the color distribution of galaxies is also strongly dependent on the absolute magnitude. Then, we can assert that the $(u - r)$ color distribution of galaxies is both related to the environment and to the luminosity of the galaxies.

These results are in agreement with Croton et al. (2005) and Einasto et al. (2005) who showed that luminosity function parameters and brightest luminosities of galaxies are smooth functions of the density of the environment.

When we take into account the morphological type of galaxies, we find that the fraction of late-type is bluer and fainter than the fraction of early-type galaxies, and that their fraction decreases from low ($0 \leq N < 4$) to dense environment ($59 \leq N < 127$), while the early-type galaxies fraction increases (Fig. 8). In particular, in the range of luminosities brighter than $M_r = -22.0$, we have an excess of early-type (75.3%) respect to late-type (1.5%) galaxies, while for low luminosities ($M_r > -21$) the fraction of late-type galaxies increases (29.8%) compared to fraction of early-type (36.0%) (Fig. 8 and Tab. 3). This result
is in accordance with the morphology-density relation (Dressler, 1980), confirming that, on average, early-type galaxies are redder, brighter, and in denser environments than late-type galaxies. It is important to notice that the \((u - r)\) color distributions for early-type and late-type galaxies, defined through the SDSS Eclass and FracDev parameters, are similar to the color distribution for PGs and SFGs, respectively (Fig. 7). Then, the environmental properties of late-type galaxies can be related to the morphology-density relation (Dressler, 1980) not only as a consequence of their morphological type, but also for their star-forming activity. This latter point is not completely unexpected. In fact, in the sample of galaxies used by Grogin & Geller (2000, 1999), there are a lot of galaxies in voids that are found in pairs or small groups. Thus, enhanced stellar formation due to tidal effects is likely to be detected among void galaxies. In a recent paper, Patiri et al. (2006) analysed the properties of voids galaxies in the SDSS-DR4, founding some results similar to ours, i.e., a bimodal distribution of the \((u - r)\) color index and a general trend for galaxies in voids to be bluer than in clusters: this latter result is strongly dependent on the absolute magnitude, as we demonstrate in this paper. In particular, they also found no difference between void and field galaxies if only galaxies in a restricted absolute magnitude range are analysed.

7. Conclusions

In this paper we analyzed the environmental dependence of galaxy population properties, looking for those features which could hint at the presence of a "void" galaxy population. The photometric properties we used in our analysis can be regarded as complementary respect to those used by other authors (Rojas et al., 2004; Hoyle et al., 2005). In particular, our density estimator allows us to exploit redshift informations, then finding galaxies in very underdense regions. We can summarize our findings in a few points:

1. Luminosity is a sensitive parameter to characterize the environmental properties of galaxies.
2. On average, a very underdense environment \((N_{\text{neigh}} \leq 4)\) is populated by galaxies which are bluer than galaxies that are in a very dense environments, \((N_{\text{neigh}} > 79)\), see Fig. 2.
3. On average, faint galaxies \((M_r > -21.0)\) are bluer in very underdense environments than in dense environments and the transition from blue to red, moving from under- to overdense environments, is more pronounced for faint galaxies \((M_r > -21.0)\), Fig. 5.
4. Although the transition from voids to clusters is more pronounced for faint galaxies, it does not seem to be a discontinuity (Fig. 4).
5. Changes in the \((u - r)\) color distribution are related to the environment, to the luminosity, and to the morphology of the galaxies. In fact, on average, fainter galaxies \((M_r > -21.0)\) are bluer, late-type and in underdense regions (voids) than brighter galaxies \((M_r < -21.0)\), which are redder, early-type and in overdense regions (clusters).
6. Galaxies classified as early-type/late-type and PGs/SFGs, according to their photometric/spectroscopic parameters and to their class of star-forming activity, have a similar \((u - r)\) color distribution (Fig. 8). Then, the environmental properties of late-type galaxies can be related to the morphology-density relation (Dressler, 1980) not only as a consequence of their morphological type, but also as a consequence of their star-forming activity.
7. We don’t find any sudden transition in the properties of "void" galaxies, respect to cluster galaxies, as suggested by Peebles (2001). On the contrary, our results show a continuity in the properties of the galaxies, from voids to clusters.

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In this appendix, we will examine how changing the environment smoothing scale with which we define the local galaxy density affects our results. To this aim, we compare the \((\rho - r)\) color distribution for the galaxies in our sample in different environments, using three different smoothing scales: 2.5 Mpc, 5 Mpc (the reference value adopted in this paper), and 10 Mpc. These values are similar to those adopted by Einasto et al. (2005). We define the underdense environment \(N < 4\) (10\textsuperscript{th} percentile) and the overdense environment for \(N > 59\) (90\textsuperscript{th} percentile), as in the paper. In the top panel of Fig. A.1 we report the color distribution for underdense (left) and overdense (right) environments, using three different smoothing scale: 2.5 Mpc, 5 Mpc (the reference value), and 10 Mpc. Finally, in the bottom panel we quantify the differences in the previous plots, that are the differences of the median \((\rho - r)\) color distribution for 2.5 and 10 Mpc respect to the reference value of of the \((\rho - r)\) color distribution for 5 Mpc adopted in the paper. These differences are plotted both for the underdense (left panel) and overdense (right panel) environments, with values \(\langle u - r \rangle - \langle u - r \rangle_{\text{ref}} < 0.03\).

The previous analysis demonstrates that the adopted value of smoothing scale (5 Mpc) is a robust representation and a good probe of both the underdense and overdense regions of the survey volume.
Fig. A.1. Top panel: the \((u - r)\) color distribution for a smoothing scale value of 5 Mpc (the reference value), in the underdense and overdense environments. Middle panel: as in the top panel, for three different values of smoothing scale: 2.5 Mpc, 5 Mpc, and 10 Mpc (left panel: underdense environments; right panel: overdense environments). Bottom panel: differences in the \((u - r)\) color distribution respect to the reference values, for different environments (left panel: underdense; right panel: overdense).