Voltage Stability Enhancement Based on Optimal Allocation of Shunt Compensation Devices Using Lightning Attachment Procedure Optimization

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ABSTRACT

This paper proposes a combined approach to determine the optimal allocation of different shunt compensation devices (shunt capacitor, static var compensator, and static synchronous compensator) in power systems. The developed approach is a combination between Lightning Attachment Procedure Optimization (LAPO) and loss sensitivity indices (LSIs). Different objective functions such as enhancement of voltage stability index, improvement of voltage profile and minimization of total power losses are considered. Two loss sensitivity indices (LSIs) are developed to reduce the search space in all buses and the total computation time. The developed algorithm is validated using standard IEEE 14-bus and IEEE 30-bus test systems. The developed algorithm succeeds to achieve the objective functions with the better performance compared with other well-known optimization techniques such as Teaching learning-based optimization (TLBO), genetic algorithm (GA) and particle swarm optimization (PSO).

KEYWORDS

Voltage Stability, Shunt Compensation Devices, Optimal Power Flow, Lightning Attachment Procedure Optimization, Sensitivity Indices.

I. INTRODUCTION

SUNT compensation is basically a powerful tool to improve voltage profile and increase the steady state transmittable power. Voltage stability problems are solved by providing sufficient reactive power at the appropriate location, thus improving the voltage profile and reducing power loss [1].

There are various kinds of shunt compensation devices and each one has its own characteristic and boundary [2]. The shunt capacitor (C), static var compensator (SVC), and static synchronous compensator (STATCOM) are used to improve the static voltage stability margin and power transfer efficiency. However, the performance of SVC and STATCOM is better in terms of reducing power losses and improving voltage profile [3]. To achieve the benefits of loss reduction and voltage profile improvement, engineers are in need to determine the optimal location and size of the shunt compensation devices.

Several techniques have been presented for solving the problem of the optimal capacitor placement in power system such as analytical, numerical programming, heuristic, artificial intelligence-based techniques [4], Combined Optimization Approach [5], Ant-lion optimization (ALO) [6, 7], Analytical Technique [8]-[10], combined algorithm based on Fuzzy Loss Sensitivity Factor with Sine Cosine Algorithm [11], combined algorithm based on Fuzzy Loss Sensitivity Factor with Teaching Learning-based Optimization (TLBO), genetic algorithm (GA) and particle swarm optimization (PSO) [12]. The genetic algorithm (GA), simulated annealing (SA), artificial immune system (AIS), Pareto Envelope-based Selection Algorithm II (PESA-II) with fuzzy logic decision maker and particle swarm optimization (PSO) have been used to determine the optimal placement of SVC in power system [13]-[14]. In [14], global harmony search algorithm (NGHS) has been used to determine the optimal allocation of STATCOM. In addition, different optimization techniques have been used for determining the optimal allocation of D-STATCOM in distribution systems [15]-[21]. However, the determination of optimal allocation of shunt compensation devices is still hot topic and needs more effort to achieve the maximum benefits from installation of these devices in electrical power systems.

This paper uses a new optimization technique, referred to as the Lightning Attachment Procedure Optimization (LAPO), to determine the optimal placement and sizing of shunt Var compensators in power systems. Lightning Attachment Procedure Optimization (LAPO) is a new optimization method that simulates the attachment procedure of lightning. LAPO has robustness, high quality and is able to disband a lot of troubles [4].

Sensitivity analysis has been applied to determine the candidate buses in order to reduce the search space in all buses and the total computation time [22]-[23].

In this paper, the optimal allocation of such compensation devices in power systems is determined using the developed optimization algorithm. In this algorithm, the candidate buses, which are considered
the most suitable buses to connect with the compensation devices, are determined based on the loss sensitivity indices (LSIs). This step is necessary for reducing the search space and computation time. Then, LAPO is applied to compute the best size and determine the appropriate kind of shunt compensation devices in power systems. The results are contrasted with modern optimization techniques such as Teaching Learning-Based Optimization (TLBO), genetic algorithm (GA) and particle swarm optimization (PSO) to confirm the applicability of the proposed technique. Two test systems are relied; the IEEE 14-bus and IEEE 30-bus system.

The rest of this paper is organized as follows: Section II presents an overview about the shunt compensation devices. The problem formulation is described in Section III. Section IV presents the sensitivity analysis. The LAPO algorithm is presented in Section V. Section VI presents the numerical results of the developed LAPO approach based on two standard test systems. Finally, the conclusions are presented in Section VII.

II. SHUNT COMPENSATION DEVICES

The capacitors are the conventional type of compensation devices that are considered relatively inexpensive. The capacitor injects reactive power and is connected in parallel with system buses. Its injected reactive power is proportional to the square of the terminal voltage. Flexible Alternating Current Transmission Systems (FACTS) are the modern type of compensation devices. They are widely used with electric power systems to improve the system loadability, security and maximize exploitation of transmission lines [24] [25]. There are different types of FACTS devices such as SVC and STATCOM.

SVC is capable to extend fast acting reactive power reparation in electrical systems. In other meaning, SVCs have their output edit for interchange inductive or capacitive current to control the voltage, power factor, harmonics and stabilizing the system. SVC includes two groups; the first group consists of a fixed capacitor (FC) and a thyristor-controlled reactor (TCR), while the second group consists of a thyristor-switched capacitor (TSC) and TCR [26] [27]. Schematic diagram of SVC is shown in Fig. 1.

STATCOM is an advanced device that depends on a power electronics voltage source converter (VSC) and it can control the injected reactive power to the system. In addition, it can extend active power when it is connected to a source of power. Schematic diagram of STATCOM is shown in Fig. 2.

![Fig. 1. SVC.](image1)

![Fig. 2. STATCOM.](image2)

Commerically, shunt compensation devices (capacitor, SVC and STATCOM) have constraints. However, this study has been achieved under injected Q with limit value 50 MVar and the suitable types of shunt compensation devices are given in Table I [14].

| Shunt controller | Qmin (MVAR) | Qmax (MVAR) |
|-----------------|------------|------------|
| Capacitor       | -10        | 10         |
| SVC             | -30        | 30         |
| STATCOM         | -50        | 50         |

III. OBJECTIVE FUNCTIONS

A. Voltage Profile Refinement

The voltage profile enhancement is the first objective function, which seeks to minimize the voltage deviations of load buses which can be represented as:

$$F_1 = \sum_{i=1}^{NPQ} (V_i - 1)$$

where, $NPQ$ is the number of load buses and $V_i$ is the voltage of load bus $i$.

B. Voltage Stability Improvement

The System stability is indicated by voltage stability index ($L_{max}$), which varies between 0 to 1. This objective function is given by:

$$F_2 = \min_{b=1,2,...,NPQ} (L_b)$$

The voltage stability index at bus $j$ is given by (3).

$$L_j = \left| 1 - \sum_{i=1}^{NPQ} F_{ij} \frac{V_i}{V_j} \right|$$

where, $V_i$ is the voltage of $i$th generator bus and $V_j$ is the voltage of load bus.

Calculate $F_{ij}$ using $Y_{bus}$ matrix (4) – (6).

$$[I_G] = [Y_{GG} Y_{GL} Y_{LG}] [V_G]$$

where, the complex voltages and currents at the load and generator are $V_G$, $V_L$, $i_L$, $i_G$. Sub-matrices of system $Y_{bus}$ are $Y_{LL}$, $Y_{GG}$, $Y_{LG}$. Eq. (4) can be written as in (5) and $F_{ij}$ is given by (6).

$$[V_L] = [Z_{LL} \ K_{GL} Y_{GG}] [I_G]$$

$$F_{ij} = [F_{ij}] = - [Y_{LG}]^{-1} [V_{LG}]$$

C. Real Power Losses Diminishing

Minimizing real power losses is the third objective function that is given by:

$$F_3 = \sum_{i=1}^{NTL} G_{ib}(V_i^2 + V_b^2 - 2V_iV_b\cos\delta_{ib})$$

where, $NTL$ is the number of transmission lines, $G_{ib}$ is the conductance of the transmission $ib$ and $\delta_{ib}$ is phase difference between voltages of buses $i$, $b$.

IV. CONSTRAINTS

A. Equivalent Constraints

The balanced load flow equations are given by:

$$P_{Gi} - P_{Di} = |V_i| \sum_{b=1}^{NPQ} |V_b| (G_{ib}\cos\delta_{ib} + B_{ib}\sin\delta_{ib})$$

$$Q_{Gi} - Q_{Di} = |V_i| \sum_{b=1}^{NPQ} |V_b| (G_{ib}\sin\delta_{ib} - B_{ib}\cos\delta_{ib})$$

where, the generated reactive and active power at bus $i$ are $Q_{Gi}$ and $P_{Gi}$.
The reactive and active load demand at bus i are $Q_i$ and $P_i$, respectively. The susceptance and conductance between buses b and i are $B_{bi}$ and $G_{bi}$, respectively.

**B. Inequality Constraints**

The inequality constraints can be classified as follows:

1. Generated active and reactive powers, generators bus voltages, voltage magnitude of load buses and transformer tap settings which are within minimum and maximum values.
2. Apparent power flow in transmission lines $\geq S_{lim}$.
3. Compensation MVAR ($-50 \leq Q_{comp} \leq 50$).

The operating constraints variables of the system must be considered in the objective functions. These variables can be easily limited in optimization solution using the quadratic penalty formulation of the objective functions for all dependent variables; therefore, the generalized objective function can be expressed as follows:

$$F_g(x, u) = f(x, u) + h_q \left( Q_{Gi} - Q_{lim} \right)^2 + h_q \sum_{i=1}^{N} \left( V_{qi} - \sqrt{P_{Gi}} \right)^2 + h_q \sum_{i=1}^{N} \left( Q_{qi} - Q_{lim} \right)^2 + h_q \sum_{i=1}^{N} \left( V_{qi} - \sqrt{P_{Gi}} \right)^2 + h_q \left( V_{qi} - \sqrt{P_{Gi}} \right)^2$$

where, $h_q$, $h_r$, $h_g$, $h_c$, $h_f$ and $h_l$ are the penalty factors. These values are positive. The highest positive values act as the limit variables of the dependent variable as:

$$x_{lim} = \{ x_{max}, x \geq x_{max} \}$$

$$x_{lim} = \{ x_{min}, x \leq x_{min} \}$$

(V. Sensitivity Analysis)

The loss sensitivity analysis consists of two LSIs to determine the candidate buses for the existence of shunt reparation devices. Consequently, the search space in all the buses, and the simulation time will be reduced. Moreover, places are arranged according to their severity for efficient detecting the candidate load buses. Fig. 3 shows two-bus system connected by a line as a part of a large power system. Buses p and q represent the sending and receiving end buses, respectively.

![Two-bus system](image)

Fig. 3. Two-bus system.

The reactive and active powers at the node p can be given as:

$$P_p = P_{eff/q} + P_{loss}$$

$$Q_p = Q_{eff/q} + Q_{loss}$$

where, the power passes through line k are $P_k$ and $Q_k$. The total reactive and active load power around bus q are $Q_{eff/q}$ and $P_{eff/q}$, respectively. The reactive and active power losses through line k are $Q_{loss/k}$ and $P_{loss/k}$, respectively.

The current passing through line k from point p to point q is given as:

$$I_k = \frac{P_{loss/k} - jQ_{loss/k}}{V_{pq} - \delta_p - \delta_q} = \frac{P_{loss/k} - jQ_{loss/k}}{R_k + jX_k}$$

where, the voltage magnitudes at point p and q are $V_p$ and $V_q$, respectively, the voltage angles at point p and q are $\delta_p$ and $\delta_q$.

The loss sensitivity analysis consists of two LSIs to determine the candidate buses for the existence of shunt reparation devices. The optimum buses to locate the shunt compensation devices are those with the highest positive values in the $LSI_i$. The optimal buses to locate the shunt compensation devices are the highest negative values in the $LSI_i$. The optimum buses where the shunt compensation devices will be located are acquired from the top two lists by means of merger or union. The buses selection is approximately half of the total number of system buses (50% to 55%).

VI. LIGHTING ATTACHMENT PROCEDURE OPTIMIZATION (LAPO)

The Lightning Attachment Procedure Optimization (LAPO) [4][28], is inspired by the nature of lightning attachment operation which contains the movement of the falling leader, spread of the rising leader, and the feature of lightning. Ultimate better result would be the lightning hit point. The suggestion method is free from any parameter setting and it is seldom stuck in the local best points.

A. Serious Phases of LAPO

1. Air Collapse on Cloud Surface

The cloud’s charges classified to three stages are shown in Fig 4. In the top stage in the cloud a large value of positive charge is placed, in the down stage in the cloud a large value of negative charge is located, as well as a little positive charge. The lightning is created and a large value of electrical charge shifts across the earth, when the voltage gradient on the border of the cloud increases, because of the potential is increased between the charge centers, the positive charges and negative charges.
2. The Fall of Lighting Channel

In the cloud’s edge air breakdown occurs, the lightning oncoming the earth in a stepwise motion. After each step, the lightning pauses, then shift to one or more other directions across the earth. With a view to know this operation, after each step, a hemisphere is seen beneath the leader tip with the center of leader tip and the radius of next step length (see Fig. 5) [4] [28]. There are more than one potential points on the face of this hemisphere, there are many of potential points which could be chosen as the next jump spot. The following jump spot is chosen randomly; yet, a spot with large value of electrical field between the line connecting the leader tip and the identical spot is more possible to be considered as the following jump.

3. Section Fading

There are a lot of spots for the following jump of lightning, the charge of the top branch is classified into new branches. The new branches are created by the same steps. No air breakdown happens when the charges of branch decrease more than a stringent value (1 μC) and the result is that no movement occurs. Thus, this branch would vanish as shown in Fig. 6.

4. Leader of the Rising

Existence of cloud implies existence of a large negative charge over the earth. This results in collecting of positive charges on the ground surface or earthed object beneath the cloud. In the heavy points, the high electric field produces air breakdown; thus, the heavy points start upward leader and spread through the air (see Fig. 7). As the downward leader is oncoming the ground, the upward leaders go across the downward leader quickly.

5. Ultimate Leaping

The ultimate jump happens when upward leader arrives to downward leader wand, the striking point would be the point from which the upward leader has started. In this situation, all the other branches disappear and charge of the cloud is naturalized through this channel.

B. Mathematical Steps of LAPO Algorithm

**First step:** Trail spot

Generated initial trail spots are placed at the cloud and earth edge. Several of these trail spots are the emitted lightning points, and some of them are the spot from which the upward leaders start. The trail spot is calculated by

\[ y_{\text{trail spot}}^i = y_{\text{min}}^i + (y_{\text{max}}^i - y_{\text{min}}^i) \times \text{rand} \]  

Where \(y_{\text{min}}\) and \(y_{\text{max}}\) are minimal and maximum bound of variables, and rand is random variable in the range (0,1). The fitness function is evaluated depending on the objective function

\[ F_{\text{trail spot}} = \text{obj} (y_{\text{trail spot}}^i) \]  

**Second step:** Jump definition

The average of all trail spots and the fitness function according to trail spot’s averages are calculated by Eqs:

\[ y_{\text{avr}} = \text{mean} (y_{\text{trail spot}}^i) \]  
\[ F_{\text{avr}} = \text{obj} (y_{\text{avr}}) \]

There are many potential spots for a test point, which the lightning can pass. Since the lightning was a random action, for test point \(i\), a random point \(p\) is chosen between the population (\(i \neq p\)). If the fitness of the point \(p\) is greater than that of the average value, the lightning leaps across this point, otherwise, the lightning shifts to another direction. And are given by

\[ y_{\text{trail spot new}}^i = y_{\text{trail spot}}^i + \text{rand} \times (y_{\text{avr}} + (y_{p\text{potential spot}}^i)) \]  

If average fitness of point \(p\) is lower than the fitness point

\[ y_{\text{trail spot new}}^i = y_{\text{trail spot}}^i - \text{rand} \times (y_{\text{avr}} + (y_{p\text{potential spot}}^i)) \]

**Third Step: Section Fading**

If the fitness function is higher than the prior point, the branch maintains; else, it fades, and are given by:

\[ y_{\text{trail spot}}^i = \begin{cases} y_{\text{trail spot new}}^i & \text{if } F_{\text{trail spot new}}^i < F_{\text{trail spot}}^i \\ y_{\text{trail spot}}^i & \text{otherwise} \end{cases} \]
This operation is executed for all the test points. In other words, in the first stage, all the remaining points are treated to shift down.

Cloud Leader connecting line to the point with higher electric field than average electric field

Leader connecting line to the point with lower electric field than average electric field

Field branches

Fig. 7. Determine the next jump and determine the lightning path.

**Fourth Step: Leader of the Rising**

As explained in the prior steps, all the test points are treated as the downward leader and shifted down. In the second stage, all the test points are treated as the upward leader and moved above. The upward leader motion depends on the charge of the channels which is essentially spread exponentially, and is given by:

\[ S = 1 - \left( \frac{j}{j_{\text{max}}} \right) \times \exp \left( -\frac{j}{j_{\text{max}}} \right) \]  

(31)

where the number of iterations is \( j \), the maximum number of iterations is \( j_{\text{max}} \), and next jump is \( s \), which depends on the charge of the channel and the next point is given by:

\[ Y_{\text{trail} \text{ new}} = Y_{\text{trail} \text{ new} + \text{rand} \times S(Y_{\text{min}} - Y_{\text{max}})} \]  

(32)

Where \( Y_{\text{min}} \) and \( Y_{\text{max}} \) are the best and the worse solutions of the population.

**Final Steps: Ultimate Leaping**

The lightning operation pauses when the up leader and the down leader are gathering each other.

### VII. Simulation Results

**A. Validation Strategy & Used Parameters**

The developed optimization technique is validated using two standard IEEE systems (IEEE 14-bus and IEEE 30-bus) with three various objective functions. The systems data are given in [29]. Three case studies are discussed for each system; (i) Case 1: One compensation device, (ii) Case 2: Two compensation devices, and (iii) Case 3: Three compensation devices.

The parameters of LAPO are population size = 20 and maximum number of iterations = 200. The parameters of TLBO are population specified size = 20 and maximum number of iterations = 200. The parameters of PSO are population size = 20, maximum iterations = 200, \( C_1 = 1.05 \), \( C_2 = 1.1 \), \( \omega_{\text{max}} = 1 \), and \( \omega_{\text{min}} = 0.3 \) [30]. The penalty factors are specified to be 100. The simulations are executed for 40 trials and the optimum results are given below.

**B. Obtained Results**

Table II and Table III present the obtained LSIs for IEEE 14-bus and IEEE 30-bus systems, respectively. The candidate buses that have high opportunity for connecting with shunt compensation devices is at the beginning of LSIs table and vice versa for the buses located at the end of LSIs table. The candidate buses are 2, 3, 4, 5, 11, 12, and 14 for IEEE 14-bus and 2, 3, 4, 5, 6, 7, 15, 16, 17, 21, 24, 26, 27, 28, and 30 for IEEE 30-bus.

**TABLE II. ORDER OF LOAD BUSES DEPENDING ON LSIS (IEEE 14-BUS TEST SYSTEM)**

| LSI_1 Order | Value | LSI_2 Order | Value |
|-------------|-------|-------------|-------|
| 2           | -0.085021 | 5           | 0.010309 |
| 5           | -0.083808 | 13          | 0.0035644 |
| 3           | -0.049055 | 14          | 0.0015991 |
| 4           | -0.025891 | 2           | 0.001478 |
| 13          | -0.022128 | 4           | 0.00026831 |
| 14          | -0.013788 | 12          | 0.00014508 |
| 12          | 0.0014145 | 11          | 0.0001217 |
| 11          | 0.00049929 | 3           | 0.00011671 |
| 10          | 0.00022395 | 10          | 8.1518e-005 |
| 1           | 0         | 1           | 0       |
| 6           | 0         | 6           | 0       |
| 7           | 0         | 7           | 0       |
| 8           | 0         | 8           | 0       |
| 9           | 0         | 9           | 0       |

**TABLE III. ARRANGEMENT OF LOAD BUSES DEPENDING ON LSIS FOR IEEE 30-BUS TEST SYSTEM**

| LSI_1 Order | Value | LSI_2 Order | Value |
|-------------|-------|-------------|-------|
| 6           | -0.24189 | 6           | 0.0047946 |
| 4           | -0.21416 | 15          | 0.0030409 |
| 2           | -0.10295 | 28          | 0.0022654 |
| 3           | -0.065464 | 2           | 0.0015673 |
| 5           | -0.062066 | 7           | 0.0010889 |
| 15          | -0.02248 | 24          | 0.00078636 |
| 30          | -0.013854 | 21          | 0.00063556 |
| 7           | -0.0089256 | 30          | 0.00058199 |
| 28          | -0.007415 | 17          | 0.00053991 |
| 27          | -0.0040301 | 27          | 0.00045571 |
| 24          | -0.003341 | 26          | 0.00028421 |
| 21          | -0.0021812 | 16          | 0.00021524 |
| 8           | -0.0020607 | 23          | 0.00016113 |
| 29          | -0.0017742 | 3           | 0.00013632 |
| 17          | -0.0017486 | 22          | 0.00013588 |
| 14          | -0.0014727 | 14          | 0.00013301 |
| 16          | -0.0010829 | 29          | 0.00012081 |
| 26          | -0.0009206 | 25          | 9.2603e-005 |
| 18          | -0.0007789 | 18          | 5.8691e-005 |
| 22          | -0.0006286 | 8           | 3.0762e-005 |
| 23          | -0.0006245 | 5           | 2.8648e-005 |
| 25          | -0.000151 | 20          | 2.0106e-005 |
| 20          | -0.0001430 | 4           | 1.3554e-005 |
| 19          | -9.9446c-01 | 19          | 6.3026c-006 |
| 1           | 0         | 1           | 0       |
| 9           | 0         | 9           | 0       |
| 10          | 0         | 10          | 0       |
| 11          | 0         | 11          | 0       |
| 12          | 0         | 12          | 0       |
| 13          | 0         | 13          | 0       |
The results obtained with LAPO are compared with those obtained by other optimization techniques. Tables IV, V and VI present the results for VSI, voltage deviation and real power losses, respectively. From these tables, it can be observed that in case of not using FACTS, the maximum voltage stability index ($L_{max}$) is 0.0669 p.u., voltage deviation is 0.0272 p.u. and active power losses is 2.8178 MW, while the maximum voltage stability index after determining the optimal allocation of different shunt compensation devices decreases from 0.0669 p.u. to 0.0645 p.u., voltage deviation decreases from 0.0272 p.u. to 0.0068 p.u. and active power losses decreases from 2.8178 MW to 2.7571 MW for IEEE 14-bus and IEEE 30-bus, in case of not using FACTS, the maximum voltage stability index ($L_{max}$) is 0.1240 p.u., voltage deviation is 0.0866 p.u. and active power losses is 3.0896 MW, while the maximum voltage stability index after determining the optimal allocation of different shunt compensation devices decreases from 0.1240 p.u. to 0.0923 p.u., voltage deviation decreases from 0.0866 p.u. to 0.0643 p.u., and active power losses decreases from 3.0896 MW to 2.8087 MW. Fig. 8 gives convergence characteristics of various optimization methods for VSI without compensation devices of IEEE 14-bus system. Fig. 9 shows the convergence characteristics of various optimization methods for power losses with one shunt compensation devices of IEEE 14-bus system. From this figure, it can be observed that the performance of developed algorithm is competing with other optimization techniques, while TLBO is considered the faster one. Fig. 10 gives the convergence characteristics of various optimization methods for power losses without shunt compensation devices of IEEE 30-bus system. From this figure, it can be observed that the performance of LAPO is competing with other optimization techniques, while GA is considered the worst one. Fig. 11 gives the convergence characteristics of various optimization methods for VSI with three shunt compensation devices of IEEE 30-bus system. It can be observed that the TLBO is the faster one compared with other optimization techniques. Fig. 12 gives convergence characteristics of various optimization methods for VSI with three shunt compensation devices of IEEE 30-bus system. Fig. 13 shows convergence characteristics of various optimization methods for VDD with three shunt compensation devices of IEEE 30-bus system. Fig. 14 gives convergence characteristics of various optimization methods for power losses with three shunt compensation devices of IEEE 30-bus system. Fig. 15 gives convergence characteristics for power losses using LAPO of IEEE 30-bus system. Fig. 16 gives convergence characteristics for VSI using LAPO of IEEE 30-bus system. From Fig. 12 and Fig. 13, it can be observed that the performance of the developed algorithm is competing with other optimization techniques.

**C. Outstanding Features of Developed Algorithm**

The results obtained by LAPO are comparable with those obtained by the well-known optimization techniques. This verifies the applicability of LAPO for power system studies as it gives a minimum objective function compared with TLBO, PSO and GA techniques.
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Fig. 13. Convergence characteristics of various optimization methods for VDD with three shunt compensation devices of IEEE 30-bus system.

Fig. 14. Convergence characteristics of various optimization methods for power losses with three shunt compensation devices of IEEE 30-bus system.

Fig. 15. Convergence characteristics for power losses using LAPO of IEEE 30-bus system.

Fig. 16. Convergence characteristics for VSI using LAPO of IEEE 30-bus system.

TABLE IV. VSI, OPTIMAL PLACEMENT, SIZE IN MVAR AND SUITABLE TYPE OF SHUNT COMPENSATION DEVICES

|                          | IEEE 14-bus system                  | IEEE 30-bus system                  |
|--------------------------|-------------------------------------|-------------------------------------|
| Without FACTS            |                                     |                                     |
| LAPO                     | 0.0669                              | 0.1240                              |
| TLBO                     | 0.0712                              | 0.12434                             |
| PSO                      | 0.0713                              | 0.1253                              |
| GA                       | 0.0715                              | 0.1257                              |
| Case 1 (value, place, size, and type) |                                     |                                     |
| LAPO                     | 0.0656, 14, 38.3232, STATCOM        | 0.1173                              |
| TLBO                     | 0.06631, 4, 49.97, STATCOM          | 0.1181                              |
| PSO                      | 0.0703, 5, 33.45, STATCOM           | 0.1251                              |
| GA                       | 0.0708, 5, 49.8751, STATCOM         | 0.1216                              |
| Case 2 (value, place, size, and type) |                                     |                                     |
| LAPO                     | 0.0648, (13, 14), (-50, 45.4927), 2 STATCOM | 0.1073, (7, 27), (9.1307, 44.8712), 2 STATCOM |
| TLBO                     | 0.0663, (4, 5), (-16.5310, 49.9692), SVC, STATCOM | 0.11312, (30, 27), (-16.7354, 50), SVC, STATCOM |
| PSO                      | 0.0701, (5, 4), (49.9997, 23.721), 2 STATCOM | 0.1168, (21, 15), (42.7866, 38.4338), 2 STATCOM |
| GA                       | 0.0664, (4, 5), (27.8177, 28.1106), 2 SVC | 0.12001, (7, 17), (-41.2411, 46.7745), 2 STATCOM |
| Case 3 (value, place, size, and type) |                                     |                                     |
| LAPO                     | 0.0645, (4, 14, 12), (-6.2314,45.0123, -50), C, 2 STATCOM | 0.0923, (15,21,30),(35.1034,22.5432,39.1089) |
| TLBO                     | 0.0655, (5, 4, 5), (30.1891, -46.0102, 43.9262), 3 STATCOM | 0.1112, (17, 21, 15), (26.174, 50.0, 35.377), SVC, 2 STATCOM |
| PSO                      | 0.0697, (4, 5, 4), (33.5932, 43.629, 30.7922), 3 STATCOM | 0.1161, (21, 7, 3), (33.6635, 49.9984, 34.6893), 3 STATCOM |
| GA                       | 0.0662, (4, 14, 4), (-24.9, 30.92, -16.123), 2 SVC, STATCOM | 0.1192, (21, 30, 15), (10.1669, 48.2160, 10.9165), C, STATCOM, SVC |
### TABLE V. Voltage Deviation in PU, Optimal Placement, Size in MVAR and Suitable Type of Shunt Compensation Devices

|                      | IEEE 14-bus system | IEEE 30-bus system |
|----------------------|--------------------|--------------------|
| **Without FACTS**    |                    |                    |
| LAPO                 | 0.0272             | 0.0866             |
| TLBO                 | 0.03211            | 0.088319           |
| PSO                  | 0.0327             | 0.0907             |
| GA                   | 0.03286            | 0.095745           |
| **Case 1 (value, place, size, and type)** |                    |                    |
| LAPO                 | 0.0148, 14, 12.2541, SVC | 0.0783, 17, 4.6421, C |
| TLBO                 | 0.0300, -42.3003, STATCOM | 0.086812, 15, 17.5913, SVC |
| PSO                  | 0.0324, 5, 43.4456, STATCOM | 0.089608, 21, 24.3424, SVC |
| GA                   | 0.0328, 4, -8.8882, C | 0.0943, 21, -41.2308, STATCOM |
| **Case 2 (value, place, size, and type)** |                    |                    |
| LAPO                 | 0.0079, (14, 12), (12.6500, -1.7732), SVC, C | 0.0779, (20, 15), (5.6523, 14.8365), C, SVC |
| TLBO                 | 0.0081, (14, 5), (13.0869, 15.3602), 2 SVC | 0.083624, (3, 24), (-14.0, 15.92), 2 SVC |
| PSO                  | 0.0083, (14, 4), (13.0757, 15.0135), 2 SVC | 0.0848, (21, 15), (4.6344, 16.8076), C, SVC |
| GA                   | 0.0183, (12, 14), (-23.9822, 11.6879), 2 SVC | 0.092047, (24, 15), (10.8060, 1.2003), SVC, C |
| **Case 3 (value, place, size, and type)** |                    |                    |
| LAPO                 | 0.0068, (4, 14, 5), (9.4621, 7.0088, 13.016), 2 C, SVC | 0.0643, (15, 26, 30), (-3.9316, 4.8339, 5.1494), 3C |
| TLBO                 | 0.00794, (12, 14, 5), (22.9890, 7.2583, 9.0851), 2 SVC, C | 0.0843, (21, 7, 15), (7.3001, 19.8402, 12.6049), C, 2 SVC |
| PSO                  | 0.0080, (14, 5), (12.9847, 24.5797, 0.6175), 2 SVC, C | 0.0911, (14, 5, 4), (12.03, -36.644, 17.7964), 2 SVC, STATCOM |
| GA                   | 0.0111, (14, 12, 5), (12.9847, 24.5797, 0.6175), 2 SVC, STATCOM | 0.0911, (30, 24, 7), (30, 4.8605, -49.9498), STATCOM, C |

### TABLE VI. Power Losses in MW, Optimal Placement, Size in MVAR and Suitable Type of Shunt Compensation Devices

|                      | IEEE 14-bus system | IEEE 30-bus system |
|----------------------|--------------------|--------------------|
| **Without FACTS**    |                    |                    |
| LAPO                 | 2.8178             | 3.0896             |
| TLBO                 | 2.8193             | 3.0997             |
| PSO                  | 2.8398             | 3.111              |
| GA                   | 2.8542             | 3.1227             |
| **Case 1 (value, place, size, and type)** |                    |                    |
| LAPO                 | 2.7922, 14.7, 3722, C | 3.0723, 11, 3046, SVC |
| TLBO                 | 2.8182, 14, -8.7037, C | 3.0772, 7, 9.7524, C |
| PSO                  | 2.8254, 5, -36.9534, STATCOM | 3.0905, 30, 44, 9121, STATCOM |
| GA                   | 2.8204, 4, 6.0963, C | 3.1137, 7, 8.6169, C |
| **Case 2 (value, place, size, and type)** |                    |                    |
| LAPO                 | 2.7603, (5, 13), (40.5023, 0.7516), STATCOM, C | 3.0625, (26, 7), (2.2619, 10.1625), C, SVC |
| TLBO                 | 2.7784, (13, 14), (8.6097, 7.1422), 2 C | 3.0632, (21, 7), (11.6681, 7.4546), SVC, C |
| PSO                  | 2.7942, (5, 13), (15.9081, 9.1433), (SVC, C) | 3.0679, (7, 21), (8.8934, 10.6073), C, SVC |
| GA                   | 2.812, (14, 5), (7.4191, -10.4339), C, SVC | 3.0932, (21, 16), (6.8264, 4.1232), 2 C |
| **Case 3 (value, place, size, and type)** |                    |                    |
| LAPO                 | 2.7571, (12, 14, 5), (1.7137, 5.306, 0.4380), C | 2.8087, (4, 21, 27), (7.9282, -3.4041, 29.0705), C, STATCOM, SVC |
| TLBO                 | 2.7599, (12, 14, 4), (22.9890, 7.2583, 9.0851), (SVC, 2 C) | 2.8712, (5, 7, 21), (45.2345, 34.6556, 23.4432), 2 STATCOM, SVC |
| PSO                  | 2.78, (14, 5, 12), (7.0831, 9.4564, 10.3951), 2 SVC | 3.0581, (30, 21, 7), (2.4394, 11.7325, 8.9302), 2 SVC, C |
| GA                   | 2.7837, (4, 14, 13), (-24.4101, 5.5066, 3.4499), SVC, 2 C | 3.082, (21, 28, 7), (15.4645, -1.1633, 8.9918), SVC, 2 C |
VIII. Conclusion

In this paper, a new hybrid optimization technique based on LAPO and loss sensitivity indices has been proposed to determine the optimal allocation of different shunt compensation devices in power systems. Two LSIs have been developed to determine the candidate locations for the existence of shunt compensation devices in order to decrease the search time in all buses and accelerate the convergence. The proposed optimization technique has been used to achieve different objective functions: voltage stability index, improvement of voltage profile and minimization of total power losses. IEEE 14-bus and IEEE 30-bus test systems have been used to verify the optimization algorithm. The results of the proposed algorithm have been compared with those obtained by other well-known optimization techniques such as TLBO, PSO and GA. The obtained results proved the capability of the proposed algorithm to effectively determine the optimal allocation of such compensation devices and achieve different objective functions during fast computation time. Other compensation devices such as UPFC, IPFC and CUPFC have not been studied using the developed technique which maybe faces some challenges with them, as they are more complex devices. Hence, the future work will be focused to solve this issue.

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References

[1] F. Dincer, “The analysis on wind energy electricity generation status, potential and policies in the world” Renewable and sustainable energy reviews 15.9 (2011): 5135-5142.
[2] P. Pourbeik, P. S. Kundur, and C. W. Taylor, “The anatomy of a power grid blackout-Root causes and dynamics of recent major blackouts” IEEE Power and Energy Magazine 4.5 (2006): 22-29.
[3] A. Sode-Yome, and N. Mithulananthan, “Comparison of shunt capacitor, SVC and STATCOM in static voltage stability margin enhancement” International Journal of Electrical Engineering Education 41.2 (2004): 158-171.
[4] A. Foroughi Nematollahi, A. Rahminejad, and B. Vahidi, “A novel physical based meta-heuristic optimization method known as Lightning Attachment Procedure Optimization” Applied Soft Computing 59 (2017): 596-621.
[5] A. Youssif, S. Kamel, M. Ebeed, and J. Yu, “Optimal Capacitor Allocation in Radial Distribution Networks Using a Combined Optimization Approach” Electric Power Components and Systems 46.19-20 (2018): 2084-2102.
[6] C. G. Botkor, A. Youssif, A. H. Ali, and S. Kamel, “Optimal Distribution Power Flow Including Shunt Capacitor Allocation Based on Voltage Deviation and Power Loss minimization” IEEE Nineteenth International Middle East Power System conference (MEPCON 2017), Cairo, Egypt, December 19-21, 2017.
[7] T. George, A. Youssif, M. Ebeed, and S. Kamel, “Ant Lion Optimization Technique for Optimal Capacitor Placement Based on Total Cost and Power Loss Minimization” IEEE International Conference on Innovative Trends in Computer Engineering (ITCE 2018), Aswan, Egypt, February 19-21, 2018.
[8] A. A. Mohamed, S. Kamel, and M. M. Aly, “A Simple Analytical Technique for Optimal Capacitor Placement in Radial Distribution Systems” IEEE Nineteenth International Middle East Power System conference (MEPCON 2017), Cairo, Egypt, December 19-21, 2017.
[9] S. Kamel, W. Hamdy, S. Abd-elgwad, A. Selim, and F. Jurado “Development of Probabilistic Power Flow Algorithm for Radial Distribution Systems with Capacitors Using Analytical Approach” IEEE 10th International Renewable Energy Congress (IREC 2019), Sousse-Tunisia, March 26-28, 2019.
[10] S. Kamel, M. Mohamed, A. Selim, L. Nasrat, and F. Jurado “Power System Voltage Stability Based on Optimal Size and Location of Shunt Capacitor Using Analytical Technique” IEEE 10th International Renewable Energy Congress (IREC 2019), Sousse-Tunisia, March 26-28, 2019.
[11] A. Selim, S. Kamel, F. Jurado, and S. Marrouchi “Power and Energy Cost Losses Minimization Using Optimal Capacitor Placement in Distribution Networks” IEEE 10th International Renewable Energy Congress (IREC 2019), Sousse-Tunisia, March 26-28, 2019.
[12] S. Kamel, A. Selim, F. Jurado, J. Yu, K. Xie and T. Wu “Capactor Allocation in Distribution Systems Using Fuzzy Loss Sensitivity Factor with Sine Cosine Algorithm” 2019 IEEE PES Innovative Smart Grid Technologies Asia (ISGT ASIA 2019), Chengdu, China, May 21-24, 2019.
[13] W. Ahmed, A. Selim, S. Kamel, J. Yu, and F. Jurado, “Probabilistic Load Flow Solution Considering Optimal Allocation of SVC in Radial Distribution System” International Journal of Interactive Multimedia and Artificial Intelligence 5.3 (2018): 152-161.
[14] R. Sirjani, A. Mohamed and H. Shareef, “Optimal allocation of shunt VAR compensators in power systems using a novel global harmony search algorithm” International Journal of Electrical Power & Energy Systems 43.1 (2012): 562-572.
[15] S. Kamel, A. Ramadon, M. Ebeed, J. Yu, K. Xie and T. Wu “Assessment Integration of Wind-based DG and DSTATCOM in Egyptian Distribution Grid Considering Load Demand Uncertainty” 2019 IEEE PES Innovative Smart Grid Technologies Asia (ISGT ASIA 2019), Chengdu, China, May 21-24, 2019.
[16] M. Abdel-Nasser, K. Mahmoud, and H. Kashef, “A Novel Smart Grid State Estimation Method Based on Neural Networks” International Journal of Interactive Multimedia and Artificial Intelligence 5.1 (2018): 92-100.
[17] A. Amin, S. Kamel, and J. Yu, “Developed Analytical Technique for Optimal Placement and Sizing of DG and DSTATCOM in Radial Distribution Systems” IEEE Twentieth International Middle East Power System conference (MEPCON 2018), Cairo, Egypt, December 18-20, 2018.
[18] M. Ebeed, S. Kamel, and H. Youssif, “Optimal Setting of DSTATCOM Based on Voltage Stability Improvement and Power Loss Minimization Using Moth-flame Algorithm” IEEE Eighteenth International Middle East Power Systems Conference (MEPCON 2016), Cairo, Egypt, December 27-29, 2016.
[19] M. A. Taher, S. Kamel, F. Jurado, and A. Ahmed “Optimal Allocation of STATCOM for Voltage Stability and System Loadability” IEEE Twentieth International Middle East Power System conference (MEPCON 2018), Cairo, Egypt, December 18-20, 2018.
[20] A. Selim, S. Kamel, and F. Jurado, “Hybrid Optimization Technique for Optimal Allocation of DG and D-STATCOM in Distribution Networks” IEEE Twentieth International Middle East Power System conference (MEPCON 2018), Cairo, Egypt, December 18-20, 2018.
[21] M. Ebeed, S. Kamel, and A. Youssif, “Optimal Integration of D-STATCOM in RDS by a Novel Optimization Technique” IEEE Twentieth International Middle East Power System conference (MEPCON 2018), Cairo, Egypt, December 18-20, 2018.
[22] B. V. Rao, and G. V. Nagesh Kumar, “Sensitivity Analysis based Optimal Location and Tuning of Static VAR Compensator using Firefly Algorithm” Indian Journal of Science and Technology 7.8 (2014): 1201-10.
[23] A. A. Abou El-Elia, R. A. El-Sehiemy, A. Kinawy and M. T. Mouwafi, “Optimal capacitor placement in distribution systems for power loss reduction and voltage profile improvement” IET Generation, Transmission & Distribution 10.5 (2016): 1209-1221.
[24] Y.-H. Song and A. Johns, “Flexible ac transmission systems (FACTS)” IEE power and energy series, London: Institution of Electrical Engineers, 1999.
[25] N. G. Hingorani and L. Gyugyi, “Understanding FACTS: concepts and technology of flexible ac transmission systems” IEEE Electrical Insulation Magazine, Wiley-IEEE press, 2000.
[26] S. Kamel, F. Jurado, and J. P. Lopes, “Optimal Placement of DSTATCOM in Distribution Systems Using Genetic Algorithm” Electric Power Systems Research 83 (2012): 157-165.
[27] S. Kamel, F. Jurado, Z. Chen, M. Abdel-Akher, and M. Ebeed, “Improved optimised unified power flow controller model in the Newton–Raphson power flow analysis using combined mismatching” IET Generation,
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References

[28] A. Foroughi Nematollahi, A. Rahiminejad, and B. Vahidi, “A novel multi-objective optimization algorithm based on Lightning Attachment Procedure Optimization algorithm” Applied Soft Computing 75 (2019): 404-427.

[29] Power systems test case archive. University of Washington, Seattle, Online: http://www.ee.washington.edu/research/pstca/

[30] R. V. Rao, V. J. Savsan and D. P. Vakharia, “Teaching–learning-based optimization: an optimization method for continuous non-linear large scale problems” Information sciences 183.1 (2012): 1-15.