Phonon-Assisted Two-Photon Interference from Remote Quantum Emitter

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ABSTRACT: Photonic quantum technologies are on the verge of finding applications in everyday life with quantum cryptography and quantum simulators on the horizon. Extensive research has been carried out to identify suitable quantum emitters and single epitaxial quantum dots have emerged as near-optimal sources of on-demand, highly indistinguishable single photons and entangled photon-pairs. In order to build up quantum networks, it is essential to interface remote quantum emitters. However, this is still an outstanding challenge, as the quantum states of dissimilar “artificial atoms” have to be prepared on-demand with high fidelity and the generated photons have to be made indistinguishable in all possible degrees of freedom. Here, we overcome this major obstacle and show an unprecedented two-photon interference (visibility of 51 ± 5%) from remote strain-tunable GaAs quantum dot emitting on-demand photon-pairs. We achieve this result by exploiting for the first time the full potential of a novel phonon-assisted two-photon excitation scheme, which allows for the generation of highly indistinguishable (visibility of 71 ± 9%) entangled photon-pairs (fidelity of 90 ± 2%), enables push-button bieexciton state preparation (fidelity of 80 ± 2%) and outperforms conventional resonant two-photon excitation schemes in terms of robustness against environmental decoherence. Our results mark an important milestone for the practical realization of quantum repeaters and complex multiphoton entanglement experiments involving dissimilar artificial atoms.

KEYWORDS: Quantum dots, quantum optics, two-photon interference, entanglement, resonant two-photon excitation

One of the very first requirements to observe ideal on-demand single photon emission is the population inversion of a two-level quantum system. Such a preparation of the quantum state is usually achieved via coherent excitation using resonant laser pulses, leading to an incoherent two-level system performing Rabi oscillations. While single-pulse resonant excitation of a quantum dot (QD) has been used to achieve high state preparation fidelities and remarkable single photon properties, this scheme cannot be used to efficiently prepare the bieexciton (XX) state, the key step to achieve polarization-entangled photon-pairs generation with QDs. This task can be instead accomplished using two-photon excitation (TPE) techniques that have recently led to the generation of on-demand entangled photon pairs. This coherent excitation scheme, however, has one important drawback. Small fluctuations in the laser pulse area or energy as well as fluctuations in the QD environment result in a strong variation of the excited state population probability that, in turn, affects the efficiency of photon generation. Envisioned quantum communication and quantum simulation applications demand instead for more robust excitation schemes, being immune against these sources of “environmental decoherence” and ensuring on-demand generation of single and entangled photon-pairs. In principle, it is possible to overcome these problems by taking advantage of the solid state nature of QDs and in particular of their coupling to acoustic phonons. Although the phonon-assisted excitation scheme is inherently incoherent, it has been proposed and recently demonstrated that population inversion of exciton (X) and XX states coupled to a quasi-continuum of vibrational modes is indeed possible. Nonetheless, the capability of this technique to generate highly indistinguishable single and entangled photons has not been explored so far. In this Letter, we show for the first time that phonon-assisted two-photon excitation of QDs allows for the generation of highly indistinguishable entangled photon-pairs. In comparison with standard excitation schemes, we
Results and Discussion. We focus our study on highly symmetric GaAs/AlGaAs QDs obtained via the droplet-etching method 16 (see Supporting Information SI Note 1). The photon-pairs emitted from this specific type of QDs have recently shown unprecedented high degree of entanglement as well as indistinguishability. 17 A typical spectrum of our highly symmetric GaAs/AlGaAs QDs under phonon-assisted excitation is shown in Figure 1a. To address the vibrational modes coupled to the XX state, the excitation laser is blue detuned by Δ from the two-phonon resonant case (Δ = 0 meV) toward the X transition (Figure 1a). The best excitation parameters for optimum state preparation are inherently determined by the materials deformation potential and QD structural details, which determine the coupling of the exciton complexes to the acoustic phonons of the solid state environment, 18 thus leading to the excitonic phonon sidebands. 18 The optimal detuning energy for the investigated type of QD system is around Δ = 0.4 meV for a pulse length of τp = 10 ps (see SI Note 2). It is important to point out that the laser energy can be swept across a range of 0.2 meV without perturbing the state preparation fidelity (5% population change, see SI Note 2), while in the conventional TPE the population varies by more than 80% on the same energetic range under π-pulse excitation (Figure 1b). The stability in the preparation fidelity versus the energy offered by the phonon-assisted scheme is particularly relevant for this work and will be later used to address remote QDs with the same laser. Before examining this point in more detail, we first discuss the robust nature of the phonon-assisted scheme in comparison with the standard TPE.

We first study the power dependence of the standard resonant TPE in the same excitation conditions and on the same QD (Figure 1c, red curve). Interestingly, the TPE manifests itself as oscillations of the state occupation probability pinned to 1/2. While a possible explanation of this effect is the presence of a chirped laser pulse in conjunction with phonon-induced damping, 9, 19 we show that it is instead connected to the detailed structure of the QD environment. The power dependence changes considerably as we additionally illuminate the QD with a weak white-light source (Figure 1c, blue curve) revealing traditional phonon-damped Rabi oscillations 20, 21 with a maximum state population as high as 88 ± 2%. We attribute these modifications (which are particularly pronounced at the π-pulse) to saturation of crystal defects located in the vicinity of the QD. In the absence of the white light, these defects release/neutralize carriers, thus giving rise to a fluctuating electric field. 22 We hypothesize that the white light not only stabilizes the electric field experienced by the QD 23 (see below) but also suppresses/saturates recombination channels (probably charged X states) that hamper the radiative recombination of the XX into the X state. Obviously, for high values of the pulse area the effect becomes negligible as the carrier-phonon interaction dominates. While the use of an incoherent above-band excitation is not generally required, many groups 24 have reported that the ensuing charge stabilization dramatically improves the state preparation fidelities when the QDs are driven resonantly. Similarly, in the sample with GaAs/AlGaAs QDs employed here, we always find that the white light leads to an increase of the maximum population probability at the π-pulse with magnitudes that are QD dependent and that range from 10% to 50% (see Figure 1c). We also point out that the intensity of the white light needed to achieve the optimal conditions is also QD-specific. Thus, strict TPE schemes are not ideal for applications in complex networks and experiments with multiple sources. In stark contrast, no remarkable effect of the white light can be observed under phonon-assisted resonant excitation (<5% change in preparation fidelity), probably due to the large laser power needed, which also stabilizes the environment. We would also like to emphasize that this is only one of the many advantages offered by the phonon-assisted excitation scheme. Beside its addressability to large laser...
detuning (see above), this scheme is inherently immune to fluctuations of the laser pulse area (see Figure 1c) due to its incoherent nature. More specifically, when the state preparation fidelity is maximum, a 10% fluctuation of the pulse area leads to a negligible (<1%) change in the state population. In the standard TPE, the same fluctuation of pulse area gives rise to at least 7% variation in the state fidelity. Finally, we emphasize that the phonon-assisted scheme allows preparing the excited state with very high fidelity, which is as high as 80 ± 2% for the highest laser pulse area available.

After demonstration of the robust nature of the phonon-assisted excitation scheme, we now investigate the quality of the generated photons in terms of entanglement fidelity and photon indistinguishability. We start out measuring the fidelity to the maximally entangled Bell state (see SI Notes 1 and 4) using a QD with small fine structure splitting (FSS) (1.3 ± 0.5 μeV). The polarization-resolved XX–X cross-correlation measurements used to estimate the fidelity are shown in Figure 2a under phonon-assisted excitation. These data yield a fidelity of f = 90 ± 2% which is identical (within the experimental error) to the values obtained when the QD is driven under strict TPE (with and without white light, Figure 2b). Therefore, the three different excitation schemes give rise to the same level of entanglement of the emitted photons. This is not surprising, as the fidelity is determined by three main contributions: (i) the relative value of the FSS with respect to the natural line width,27 (ii) recapture processes3 increasing the multiphoton emission and (iii) the hyperfine interaction.30,31 Because the lifetime (i) as well as the single photon purity (ii) and the hyperfine interaction (iii) are not affected by the excitation scheme (see SI Note 3), the fidelity to the Bell state is expected to remain constant, as indeed confirmed experimentally (Figure 2b).

The different excitation methods are instead expected to have a pronounced role in the indistinguishability of consecutive photons emitted by the same QD, as measured in a Hong–Ou–Mandel type experiment22 on the XX and X photons. The time delay between consecutive photons was set to 2 ns via a Mach–Zehnder interferometer in the excitation path. The observation of the typical two-photon interference quintuplet is presented in Figure 3, together with the visibility values $V_X$ and $V_{XX}$ which are calculated taking into account the imperfections of the interference beam splitter and are referenced to the next neighboring side-peaks (see SI Notes 1 and 5). If we first take a look at the standard TPE (Figure 3a), we observe visibilities of 60% for both, XX and X photons, on the arbitrarily chosen QD. In particular, we would like to emphasize that the studied QD was selected randomly and that QDs with much higher visibilities can be found on the very same sample. The stabilization of the QD environment throughout illumination with the white light source (Figure 3b), however, leads to an evident (slight) increase of the X (XX) visibility. This is reasonable as the X is more sensitive to spectral diffusion mediated by temporally charged defects22 than the screened potential of the fully occupied XX state. The weaker visibility of the XX transition, on the other hand, can be related to the XX probing an extraordinary noise environment32 and/or suffers from an initially higher pure dephasing rate.34 Most importantly, under phonon-assisted excitation of the two-level system (Figure 3c) a remarkably high level of indistinguishability (comparable to the TPE under white light illumination) can be observed. This demonstrates that the time jitter introduced by phonon relaxation has a negligible impact on our measured values of photon indistinguishabilities. This result is particularly relevant for applications, as the lifetime of the X and XX transitions in our GaAs QDs are very similar to the values reported for near-optimal single photon sources exploiting the Purcell effect and based on InAs QDs.35,36 Therefore, the fact that we do not observe a degradation in the phonon indistinguishability suggests that the phonon-assisted excitation scheme may be readily adopted in systems showing the best performances in terms of indistinguishability and brightness.37 To summarize, the phonon-assisted two-photon excitation scheme not only leads to the generation of highly indistinguishable entangled photon-pairs but it is more robust than the standard two-photon excitation schemes. Yet, this
scheme has an additional elegant advantage: it allows performing two-photon interference between remote QDs driven by the same pulsed laser of fixed frequency. This is a direct consequence of the wide range of laser detunings that allows achieving the maximum population inversion and it is in contrast to the traditional two-photon excitation schemes, which instead require a precise control of the laser energy for each individual QD. Since our QDs feature similar (albeit not identical) XX binding energies, the phonon-assisted two-photon excitation is a universal clocked excitation for arbitrary large numbers of QDs, hence a scalable approach for quantum optics.

The excitation of the remote emitters is timed so that the individual single photons from the two QDs, depicted as ice cubes in Figure 4a, overlap on a beam splitter (BS2) performing two-photon interference. For this experiment, we placed a second sample on top of a piezoelectric actuator to provide strain-tunability of the QD emission lines38−40 (see Methods) and to ensure frequency matching of the photons impinging at BS2. Two X transitions with almost identical lifetimes and high single photon purity from two remote QDs (see SI Note 6) are tuned to the same frequency by applying a voltage across the piezoelectric actuator mounted below QD A (Figure 4b). We stress once more that the standard TPE cannot be used to drive efficiently the two QDs, as the XX binding energies differ by more than 0.1 meV (see the discussion above). Under phonon-assisted TPE we can instead prepare the two QDs with the highest probability by simply finding the optimum laser detuning for both, which in this special case turns out to be $\Delta = 0.36$ meV at a pulse area of $5\pi$ on each setup (Figure 1b), a value that is limited only by the power available in our experiment. The resulting correlation measurements are depicted in Figure 4c for the cross- and copolarized configurations. In contrast to the two-photon interference of consecutive photons from a single source, where the cross-polarized configuration always yields a value comparable to the side-peaks (see SI Note 5), this condition is not necessarily realized when combining remote single photon sources. In particular, long time-scale blinking (which may be due to random QD charging and consequent suppression of resonant absorption) reduces the value of $g^{(2)}(0)$ even when the average intensities of the two emitters are kept the same.41 Thus, it is crucial to first determine the cross-polarized correlation and to evaluate the real remote two-photon interference visibility $V_{\text{remote}}$ as follows

$$V_{\text{remote}} = \frac{g^{(2)}_{\perp}(0) - g^{(2)}_{\parallel}(0)}{g^{(2)}_{\parallel}(0)}$$

(1)

The optimized value for the overlap of the individual photon energies is then found by sweeping the X transition of QD A in steps of voltages that modify the energy on the order of a fraction of the line width, as demonstrated in Figure 4d. By doing so we report on a remote interference visibility as high as $V_{\text{remote}} = 51 \pm 5\%$, the highest value ever observed for QDs38,42−44 without the need of any temporal/spectral selection. So far only coherently scattered45 or Raman photons46 from remote QDs achieved higher two-photon interference visibilities. However, these excitation schemes cannot be used to generate pairs of photons and do not allow
for the on-demand state preparation, both important prerequisites for quantum relays based on entangled photons from QDs. The measured visibility is in good agreement with the theoretical limits obtained from Michelson interferometry. Using a reported model and the QD parameters estimated in the experiment (see SI Note 6) we calculate that the maximum visibility achievable in the experiment is 56%, a value which is very close to the experimental one. Currently we are only able to choose the proper QDs, probably due to charge noise and phonon sidebands, as we do not apply any spectral filtering in our measurement. A possible way to overcome these problems is to use devices that enable the application of electric fields and/or photonic cavities to shorten the lifetime of the transition via the Purcell effect, so as to effectively filter out the phonon sidebands.

In conclusion, we performed two-photon interference between photons emitted by two remote QDs with a visibility of 51 ± 5%, by using the full power of the novel phonon-assisted two-photon excitation scheme. In a comprehensive study, we compare different resonant excitation schemes and show that the phonon-assisted state preparation is a robust method to generate on-demand single pairs of highly entangled and indistinguishable photons from semiconductor quantum dots. It is interesting to note that this is the first report on two-photon interference using remote GaAs QDs and that the first (unsuccessful) attempt to observe this phenomenon with solid-state systems was also based on GaAs QDs in nanoholes. The proper choice of the QD growth strategy, of the energy-tuning method, and, most notably, of the excitation scheme paves the way toward entanglement swapping experiments between independent QDs and other complex multisource experiments.

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**ASSOCIATED CONTENT**

* Supporting Information
  The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.nanolett.7b00777.

  Methods, detuning parameters of the phonon-assisted TPE; lifetime and autocorrelation; fidelity evaluation; two-photon interference using the same QD; two-photon interference from remote QDs (PDF)

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M.R., K.D.J., and D.H. performed the measurements with the help from C.S. and R.T. M.R. made the data analysis with the help from K.D.J., D.H., and R.T. Y.H. grew the sample with advice of A.R. C.S. processed the sample. M.R., K.D.J., and R.T. wrote the manuscript with the help from all the authors. R.T. conceived the experiment and supervised the project.

**Notes**
The authors declare no competing financial interest.
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