Revisiting gravitino dark matter in thermal leptogenesis

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Abstract

In this paper, we revisit the gravitino dark matter scenario in the presence of the bilinear $R$-parity violating interaction. In particular, we discuss a consistency with the thermal leptogenesis. For a high reheating temperature required for the thermal leptogenesis, the gravitino dark matter tends to be overproduced, which puts a severe upper limit on the gluino mass. As we will show, a large portion of parameter space of the gravitino dark matter scenario has been excluded by combining the constraints from the gravitino abundance and the null results of the searches for the superparticles at the LHC experiments. In particular, the models with the stau (and other charged slepton) NLSP has been almost excluded by the searches for the long-lived charged particles at the LHC unless the required reheating temperature is somewhat lowered by assuming, for example, a degenerated right-handed neutrino mass spectrum.

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I. INTRODUCTION

For decades, supersymmetry has been widely studied as one of the top candidates for physics beyond the Standard Model (SM) which allows a vast separation of low energy scales from high energy scales such as the Planck scale. The precise unification of the gauge coupling constants at the scale of the grand unified theory (GUT) also strongly supports the minimal supersymmetric standard model (MSSM). In addition, when the $R$-parity \cite{1} is imposed to forbid baryon ($B$) and lepton ($L$) number violating interactions, the lightest supersymmetric particle (LSP) becomes a good candidate for dark matter.

Although the $R$-parity is very important phenomenologically, understanding of its origin remains as an open question \cite{2}. In fact, in view of general discussion that all global symmetries are necessarily broken by quantum gravity effects \cite{3–8}, the $R$-parity is potentially violated unless it is embedded in gauged symmetries\footnote{1 Discrete subgroups of the gauge symmetries are immune to quantum gravitational effects \cite{9–12}.}

A popular framework for such embedding is to identify the $R$-parity (or the matter parity \cite{13–16}) with a discrete $\mathbb{Z}_2$ subgroup of the gauged $U(1)_{B-L}$ symmetry, which naturally emerges once we introduce right-handed neutrinos required for the seesaw mechanism \cite{17} \cite{18} \cite{see also 19}. There, the Majorana masses of the right-handed neutrinos are induced when the $U(1)_{B-L}$ symmetry is broken down to its $\mathbb{Z}_2$ subgroup spontaneously.

This framework is, however, known to have a tension with perturbative $SO(10)$ GUT. There, the Majorana mass terms of the right-handed neutrinos require the vacuum expectation value (VEV) of fields in $\mathbf{126}$ or larger representations of $SO(10)$. However, an introduction of fields in such large representations causes a rapid blow up of the $SO(10)$ gauge coupling constant just above the GUT scale. To avoid this problem, it is often assumed that $U(1)_{B-L}$ by a VEV of $\mathbf{16}$ representation with which the Majorana masses are given by $\langle \mathbf{16} \rangle^2$. In this case, the $\mathbb{Z}_2$ subgroup of $U(1)_{B-L}$ does not remain unbroken, and hence, no exact $R$-parity remains\footnote{2 See \cite{20} for a recent discussion on $R$-parity violation in string theory.} Rather, this argument opens up a new framework\footnote{3 This does not preclude the $R$-parity originating from symmetries other than $U(1)_{B-L}$ though.} where small $R$-parity violation effects are tied with $U(1)_{B-L}$ breaking as pursued in Refs. \cite{21, 22}.

Once $R$-parity violation is accepted, the gravitino LSP has a definite advantage to be
a candidate for dark matter. Compared with other LSP candidates, the gravitino LSP can have a much longer lifetime even in the presence of $R$-parity violation \cite{23, 24}.

In this paper, we discuss gravitino dark matter in the presence of the $R$-parity violating interactions. In particular, we revisit a consistency with the thermal leptogenesis \cite{25} \cite[see 26–28 for review]{26, 28}. For a high reheating temperature required for the thermal leptogenesis, the gravitino dark matter tends to be overproduced, which puts a severe upper limit on the gluino mass \cite{21, 29, 30}. As we will show, a large portion of parameter space of the gravitino dark matter scenario has been excluded by combining the constraints from the gravitino abundance and the null results of the searches for the superparticles at the LHC experiments.

The organization of this paper is as follows. In Sec.\[II\] we briefly review $R$-parity violation in the MSSM. We also review the gravitino properties in the presence of $R$-parity violation. In Sec.\[III\] we discuss a consistency between the gravitino dark matter scenario and thermal leptogenesis scenario. There, we also discuss the constraints from the LHC experiments. Final section is devoted to our conclusions and discussions.

\section{R-Parity Violation and the Gravitino Dark Matter}

Let us briefly review $R$-parity violation in the MSSM (see \cite{31} for a detailed review). The general renormalizable $R$-parity violating superpotential is given by

$$W_R = \frac{1}{2} \lambda_{ijk} L_{Li} L_{Lj} \bar{E}_{Rk} + \lambda'_{ijk} L_{Li} Q_{Lj} \bar{D}_{Rk} + \frac{1}{2} \lambda''_{ijk} \bar{U}_{Ri} \bar{D}_{Rj} \bar{D}_{Rk} + \mu'_{i} L_{Li} H_u,$$

where $i, j, k = 1, 2, 3$ denote the family indices of the matter fields. The coefficients $\lambda^{(r, u)}$ and $\mu'$ are dimensionless and dimensionful parameters of $R$-parity violation, respectively. The third term violates the $B$-number while the other terms violate the $L$-number.

The most universal constraints on $R$-parity violation come from cosmology. In the presence of the $B$ and/or $L$-number violating processes induced by $R$-parity violation, the baryon asymmetry generated before the electroweak phase transition would be washed out. To avoid this problem, the $R$-parity violating parameters are constrained to be

$$\lambda, \lambda', \lambda'', \mu'/\mu < \mathcal{O}(10^{-(6-7)}) ,$$

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where $\mu$ denotes the $R$-parity conserving $\mu$-parameter in the TeV range $32-35$. Hereafter, we suppress the family indices for simplicity.

The bilinear $R$-parity terms in Eq. (1) are also constrained from the neutrino mass $31$. By taking the cosmological upper limit on the neutrino mass, $\sum_i m_{\nu_i} \lesssim 0.183$ eV (at 95% CL) $39$, the constraint is given by,

$$\sum_i \frac{\mu'^2_i}{\mu^2} \lesssim 2 \times 10^{-11} \tan^2 \beta \left( \frac{M_2}{1 \text{ TeV}} \right) \left( \frac{M_1}{M_1 c_W^2 + M_2 s_W^2} \right). \quad (3)$$

Here, $M_{1,2}$ are the soft supersymmetry breaking masses of the bino and the wino, respectively, $\tan \beta$ is the ratio between the VEVs of the two Higgs doublets, and $s_W^2$ denotes the weak mixing angle, $\sin^2 \theta_W$, with $c_W^2 = 1 - s_W^2$. It should be noted that we take the basis of the Higgs bosons and the sleptons, $(H_d, \tilde{L}_i)$, so that no sleptons obtain VEVs (see $31$ for details).

Now, let us briefly discuss $R$-parity violation tied to $U(1)_{B-L}$ breaking. In particular, we focus on models where the effects of $R$-parity violation in the MSSM appear through tiny VEVs of the right-handed neutrinos, $\langle \bar{N}_R \rangle$ $22, 40$ (see also the appendix A). In this class of models, the $R$-parity violating parameters are generated as

$$\mu' \sim y_{\nu} \langle \bar{N}_R \rangle. \quad (4)$$

Thus, the constraints in Eqs. (2) and (3) on $\lambda^{(0)}$ and $\mu'$ can be satisfied as long as $\langle N_R \rangle$'s are small.

As an advantageous feature of this class of models, the $B$-violating term, $\lambda''$, can be further suppressed by additional symmetries (see the appendix A). Thus, this class of models can evade the sever constraints from the null observation of proton decay $31$,

$$|\lambda' \lambda''| \lesssim 10^{-25} \left( \frac{m_{\text{SUSY}}}{1 \text{ TeV}} \right)^2, \quad (5)$$

where $m_{\text{SUSY}}$ denotes a typical mass of superparticles.

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4 See Ref. $36$, for baryogenesis $37, 38$ in the presence of the $R$-parity violation.
5 In the basis of $(H_d, \tilde{L}_i)$ where no sleptons obtain VEVs, the trilinear terms are also generated as $\lambda \sim \lambda' \sim \mu'/\mu$. 

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mainly decays into a pair of a $Z$ boson and a neutrino, a pair of a Higgs boson and a neutrino, and a pair of a $W$ boson and a charged lepton. The relative branching ratios into those modes converge to $1:1:2$ in the limit of $m_{3/2} \gg m_{Z,W,h}$\[^{[41, 42]}\]. The decay widths of those modes are roughly given by,

$$2\Gamma[\psi_{3/2} \to Z\nu] \sim 2\Gamma[\psi_{3/2} \to h\nu] \sim \Gamma[\psi_{3/2} \to W\ell] \sim \frac{m_{3/2}^3}{192\pi M_{PL}^2} \left(\frac{\mu'}{\mu}\right)^2,$$

leading to the lifetime of the gravitino,

$$\tau_{3/2} \simeq 10^{20} \text{ sec} \times \left(\frac{1 \text{ TeV}}{m_{3/2}}\right)^3 \left(\frac{10^{-7}\mu}{\mu'}\right)^2.$$

Here, $m_{3/2}$ denotes the gravitino mass, and $M_{PL} \simeq 2.4 \times 10^{18} \text{ GeV}$ the reduced Planck scale. Therefore, the lifetime of the gravitino can be much longer than the age of the universe, $\mathcal{O}(10^{17})$ sec, for $\mu'/\mu \ll 10^{-7}$ for the gravitino in the hundreds GeV to a TeV range.

The gravitino lifetime in the range of Eq. (7) is, however, severely constrained from the observation of the extragalactic gamma-ray background (EGRB)\[^{[43–46]}\]. By using 50-month EGRB observation by Fermi-LAT\[^{[48]}\], the lifetime of the gravitino dark matter decaying into a pair of a $W$ boson and a charged lepton is constrained to be $\tau_{3/2} \gtrsim 10^{28}$ sec for $m_{3/2} = \mathcal{O}(100 \text{ GeV–1 TeV})$. In the following, we assume that the bilinear $R$-parity violating parameters satisfy

$$\frac{\mu'}{\mu} \lesssim 10^{-11} \times \left(\frac{1 \text{ TeV}}{m_{3/2}}\right)^{3/2}.$$

\[^{6}\] The observations of the neutrino fluxes also constraints the lifetime of the gravitino, which is less stringent than those from the EGRB\[^{[47]}\].
III. GRAVITINO DARK MATTER IN THERMAL LEPTOGENESIS SCENARIO

A. Thermal gravitino production

The productions of the gravitino from the thermal bath are dominated by the QCD process. The resultant relic density of the gravitino dark matter is given by [49, 50],

\[ \Omega_{3/2} h^2 \simeq 0.09 \left( \frac{m_{3/2}}{100 \text{ GeV}} \right) \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \left( 1 + 0.558 \frac{r_{\bar{g}}^2 m_{\bar{g}}^2}{m_{3/2}^2} \right) 
- 0.011 \left( 1 + 3.062 \frac{r_{\bar{g}}^2 m_{\bar{g}}^2}{m_{3/2}^2} \right) \log \left( \frac{T_R}{10^{10} \text{ GeV}} \right) \right), \tag{9} \]

for the universal gaugino mass generated at the GUT scale. Here, the parameter \( r_{\bar{g}} \) is introduced to translate the universal gaugino mass parameter, \( m_{1/2} \), at the GUT scale to the physical gluino mass, \( m_{\bar{g}} \),

\[ m_{\bar{g}} = r_{\bar{g}} m_{1/2} \, , \tag{10} \]

which depends on the MSSM parameters. In our analysis, we fix \( r_{\bar{g}} = 2.5 \) for simplicity, which reproduces the gluino mass with an accuracy of 10% for wide range of the MSSM parameters. It should be noted that the relic density in Eq. (9) is about a factor two larger than the one in [29] which is caused by the thermal mass effects of the gluon as discussed in [49].

From the relic density in Eq. (9), we immediately find that the gluino mass is severely constrained from above for successful leptogenesis which requires a high reheating temperature, \( T_R \gtrsim 1.4 \times 10^9 \text{ GeV} \) [52]. Here, we assume that the spectrum of the right-handed neutrinos are not degenerated. In Fig. 1, we show the upper limits on the gluino mass for given reheating temperatures. In the figure, the gray shaded regions are excluded where the gravitino relic density exceeds the observed dark matter density, \( \Omega h^2 \simeq 0.1198 \pm 0.0015 \) [53]. The dark matter density can be fully explained on the upper limit on the gluino mass for a given gravitino mass. The figure shows that the upper

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7 Electroweak contributions to the gravitino production increases the abundance by around 20% when the gaugino masses satisfy the GUT relation [51].

8 The definitions of the reheating temperature in [26, 52] and in [50] are slightly different and the former is about 30% larger for a given inflaton decay width.
The upper limits on the gluino mass as a function of the gravitino mass, \( m_{3/2} \), for given reheating temperatures. Below the black dashed lines, the gravitino becomes heavier than the gluino. The gray shaded regions are excluded where the gravitino abundance exceeds the observed dark matter abundance. The gaugino masses can satisfy the GUT relation in the left side of the red dashed line while keeping the gravitino being the LSP.

The limit on the gluino mass is around 1.5 TeV for \( T_R \gtrsim 1.4 \times 10^9 \text{GeV} \). In the right panel of Fig. 1, we also show the upper limit on the gluino mass for \( T_R \simeq 10^9 \text{GeV} \) in case that the reheating temperature required for leptogenesis is somewhat relaxed.

Let us comment here that the constraints become much severer when the gaugino masses satisfy the GUT relation,

\[
m_\tilde{b} : m_\tilde{w} : m_\tilde{g} \sim 1 : 2 : 5 - 6 ,
\]

where \( m_{\tilde{b}, \tilde{w}} \) are the masses of the bino and the wino, respectively. When the GUT relation is satisfied, the gravitino mass should be smaller than the bino mass

\[
m_{3/2} < m_\tilde{b} \simeq \frac{1}{5} m_\tilde{g} ,
\]

so that the gravitino is the LSP. In Fig. 1, this condition can be satisfied only in the left side of the red dashed line. There, the limits on the gluino mass are \( m_\tilde{g} \lesssim 1.3 \text{ TeV} \) for \( T_R > 1.4 \times 10^9 \text{GeV} \) and \( m_\tilde{g} \lesssim 1.8 \text{ TeV} \) for \( T_R > 10^9 \text{GeV} \), respectively.

In the right side of the red dashed line, on the other hand, the bino and the wino should be heavier than the GUT relation in order for the gravitino to be the LSP. Since the heavier bino/wino masses increase the electroweak contributions to the gravitino abundance, the abundance in Eq. (9) underestimates the gravitino abundance in this region. Therefore,
the upper limit on the gluino mass in the right side of the red dashed line is rather conservative.

B. NLSP contributions

As discussed in [54–56], the late-time decay of the next-to-lightest superparticle (NLSP) also contributes to the relic gravitino density,

\[ \Omega_{3/2}^2 h^2 = \Omega_{3/2}^2 h^2 + Br_{3/2} \times \frac{m_{3/2}}{m_{\text{NLSP}}} \Omega_{\text{NLSP}} h^2. \]  

(13)

Here, \( \Omega_{\text{NLSP}} \) denotes the thermal relic density of the NLSP when it is stable, and \( Br_{3/2} \) the branching fraction of the NLSP into the gravitino. In the absence of \( R \)-parity violation, the NLSP dominantly decays into the gravitino, and hence, \( Br_{3/2} = 1 \). In this case, the constraints on the gluino mass from the gravitino abundance in Fig. 1 are severer [55, 57].

In the presence of \( R \)-parity violation, on the contrary, \( Br_{3/2} \) can be much suppressed when the effects of \( R \)-parity violation are sizable. In fact, the width of the \( R \)-parity violating decay (via the bilinear \( R \)-parity violating terms) is roughly given by,

\[ \Gamma_{\text{NLSP}}^R \approx \frac{\kappa}{16\pi} \left( \frac{\mu'}{\mu} \right)^2 m_{\text{NLSP}}, \]  

(14)

which leads to the lifetime,

\[ \tau_{\text{NLSP}} \approx 10^{-4}\text{sec} \times \kappa^{-1} \left( \frac{10^{-11}\mu}{\mu'} \right)^2 \left( \frac{1 \text{ TeV}}{m_{\text{NLSP}}} \right). \]  

(15)

Here, \( \kappa \) represents dependences on the MSSM parameters [21–41]. This width is much larger than the width of the \( R \)-parity conserving decay into a pair of the gravitino and the superpartner of the NLSP,

\[ \Gamma_{\text{NLSP}}^R \approx \frac{1}{4\pi} \frac{m_{\text{NLSP}}^5}{m_{3/2}^2 M_{\tilde{P}L}^2}, \]  

(16)
which corresponds to

\[ \tau_{NLSP}^R \approx 5 \times 10^3 \text{sec} \left( \frac{m_{3/2}}{100 \text{GeV}} \right)^2 \left( \frac{1 \text{TeV}}{m_{NLSP}} \right)^5. \]  

(17)

Therefore, \( Br_{3/2} \) is expected to be very small even for small \( R \)-parity violating bilinear terms as in Eq. (18).

It should be also noted that the properties of the NLSP are strongly constrained by Big-Bang nucleosynthesis (BBN) [59, 60]. For the neutralino NLSP, for example, the lifetime should be shorter than \( 10^2 \) sec to avoid dissociation of the light elements by the NLSP decays into hadronic showers (especially into nucleons). For the stau NLSP, on the other hand, the lifetime should be shorter than \( 10^{3-4} \) sec to avoid the light element dissociation. By taking those constraints from the BBN into account, we assume that the \( R \)-parity violating parameters are in the range of,

\[ 10^{-14} \times \kappa^{-1/2} \left( \frac{1 \text{TeV}}{m_{NLSP}} \right)^{1/2} \lesssim \frac{\mu'}{\mu} \lesssim 10^{-11} \times \left( \frac{1 \text{TeV}}{m_{3/2}} \right)^{3/2}. \]  

(18)

In the appendix A, we show a model which leads to the bilinear \( R \)-parity violation terms in this range. It should be noted that \( Br_{3/2} \ll 1 \) in this range of \( R \)-parity violation, and hence, the NLSP contribution to the gravitino abundance in Eq. (13) is negligible.\(^9\)

\[ C. \text{ Collider Constraints} \]

In this subsection, we discuss the constraints from the superparticle searches at the LHC. First, let us note that the \( R \)-parity violating parameters we are interested in are small and we can apply the search strategies for the superparticles at the LHC in the \( R \)-conserving case.\(^10\) In fact, for the neutralino NLSP, the lifetime is typically given by [21, 41],

\[ c \tau_{\tilde{\chi}_1^0} \gtrsim 10^6 \text{m} \times \left( \frac{1 \text{TeV}}{m_{\tilde{\chi}_1^0}} \right)^3 \left( \frac{10^{-11} \mu}{\mu'} \right)^2 \left( \frac{10}{\tan \beta} \right)^2. \]  

(19)

\(^9\) For typical size of \( \Omega_{NLSP} h^2 \), see [55].

\(^{10}\) See also [61] for the effects of \( R \)-parity violation on the LHC search for much lighter gravitinos.
FIG. 2. Left) The constraints on \((m_{\tilde{\chi}^0_1}, m_{\tilde{g}})\) from the searches for multi-jets with missing momentum extracted from [62]. Right) The constraints on \((m_{\tilde{\tau}}, m_{\tilde{g}})\) from the searches for long-lived charged particles. The constraint on the stau production cross section in [63] is converted to the gluino mass bound by using the gluino production cross section (reduced by 2\(\sigma\) theoretical uncertainties) in [64]. The region with \(m_{\tilde{\tau}} < 340\) GeV is also excluded by the long-lived charged particle searches by assuming direct stau production [63]. In both panels, we assume that the squarks are heavy and decoupled.

For the stau NLSP, on the other hand, the lifetime is similarly given by [21, 41],

\[
 c\tau_{\tilde{\tau}} \gtrsim 10^7 \text{m} \times \left(\frac{1\text{TeV}}{m_{\tilde{\tau}}}\right) \left(\frac{10^{-11}\mu}{\mu'}\right)^2 \left(\frac{10}{\tan\beta}\right)^2 .
\]  

Therefore, the NLSP is stable inside the detectors in both cases.

Let us begin with the collider constraints in the case of the neutralino NLSP. Since the neutralino NLSP is stable inside the detectors, we consider the searches for multi-jets with missing momentum. To derive conservative limits on the gluino mass, we assume that all the squarks are heavy and decoupled. In Fig.2 we show the constraints on the gluino mass and the neutralino mass at the 95% CL which are extracted from the results by the ATLAS collaboration [62]. Here, the gluino is assumed to decay into two quarks and a neutralino for simplicity. The figure shows that the lower limit on the gluino mass

\footnote{See also [65], for the constraints put by the CMS collaboration.}
is around 1.8 TeV when the neutralino is not degenerated with the gluino. When the neutralino mass is close to the gluino mass, the constraints become weaker though the gluino mass below 1 TeV is excluded unless the neutralino is highly degenerated with the gluino.

For the stau NLSP, on the other hand, we consider the long-lived charged particle searches. So far, the CMS collaboration puts a lower limit on the mass of the long-lived stau, $m_{\tilde{\tau}} > 340$ GeV at 95% CL, by assuming a direct Drell-Yan stau pair production. The CMS collaboration also puts upper limits on the production cross section of the stau pairs for a given stau mass. Since the stau production cross section (including the one from the cascade decays of the gluinos) depends on the gluino mass, we can put constraints on the gluino mass for a given stau mass. In Fig. 2, we show the resultant constraints on $(m_{\tilde{\tau}}, m_{\tilde{g}})$ plane. Here, we obtain the constraints by comparing the 95% CL limits on the stau production cross section in [63] with the gluino production cross section in [64]. The light shaded region denotes the excluded region for the central value of the gluino production cross section in [64], while the darker shaded region denotes the one for the cross section reduced by $2\sigma$ theoretical uncertainties. In the following analysis, we use the later constraint for conservative estimation.

Now, let us combine the constraints from the gravitino abundance in Fig. 1 with the constraints in Fig. 2 from the collider searches. In Fig. 3, we show the constraints in the case of the neutralino NLSP on the $(m_{\tilde{\chi}^0_1}, m_{3/2})$ plane. The figure shows that large portion of the parameter region has been excluded by the LHC constraints for successful leptogenesis, i.e. $T_R \gtrsim 1.4 \times 10^9$ GeV. Even for somewhat relaxed requirement, $T_R \gtrsim 10^9$ GeV, some portion of the parameter region has been excluded by the LHC results. The remaining allowed region will be tested for 300 fb$^{-1}$ of integrated luminosity at 14 TeV which reaches to $m_{\tilde{g}} \simeq 2.8$ TeV [66]. If we assume the GUT relation to the gaugino masses, the parameter region has been excluded even for somewhat lower reheating temperature $T_R \gtrsim 10^9$ GeV.

In Fig. 4, we also show the combined constraints for the stau NLSP. The figure shows that all the parameter region has been excluded by the LHC constraints for $T_R \gtrsim 1.4 \times 10^9$ GeV.

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12 In our analysis, we require that the dark matter density is dominated by the gravitino density. Hence, we assume that the gluino mass should lie on the upper limit in Fig. 1 for a given gravitino mass.
FIG. 3. Combined constraints for the neutralino NLSP. The reheating temperature is assumed to be $T_R = 1.4 \times 10^9$ GeV (left) and $T_R = 10^9$ GeV (right). The gray shaded regions are excluded where the gravitino is no more the LSP. The blue shaded regions are excluded by the missing momentum searches \cite{62, 65}. The GUT relation of the gaugino mass can be satisfied in the left side of the red dashed line. The horizontal dashed lines show the upper limit on the gluino mass for a given gravitino mass shown in Fig. 1.

$10^9$ GeV. For a relaxed requirement, $T_R \gtrsim 10^9$ GeV, on the other hand, there remains some allowed region, which can be also tested by further data taking.

So far, we have discussed the cases with the neutralino NLSP and the stau NLSP. Before closing this section, let us comment on other candidates for the NLSP. When the gluino is the NLSP, it is again stable inside the detectors, and is hadronized with the SM quarks to form the so-called $R$-hadrons \cite{67, 68}. The $R$-hadrons are charged unless the gluinos are bounded with the gluons, and the charged $R$-hadrons can be searched for as long-lived charged particles. So far, the CMS collaboration has excluded the gluino mass below 1.5 TeV at 95% CL when the 50% of the $R$-hadrons are assumed to be charged \cite{63}.\footnote{When the 90\% of the $R$-hadrons are assumed to be charged, the constraints becomes $m_{\tilde{g}} < 1.59$ TeV.} Thus, by comparing with the upper limit on the gluino mass in Fig. 1 we find that the gravitino dark matter cannot be consistent with the thermal leptogenesis as in the case with the stau NLSP, unless the required reheating temperature is somewhat lowered.

The CMS collaboration also puts constraints on the production cross section of the
As for the other charged NLSPs such as selectron/smuon/charginos, the same constraints with the stau NLSP can be applied. For the sneutrino NLSP, on the other hand, it leaves missing momentum inside the detector as in the case of the neutralino NLSP. However, we need to perform more detailed analyses including model building to derive constraints, since the event topologies depend on the decay patterns of the gluinos into the sneutrinos. In addition, some careful parameter tunings are required to achieve the sneutrino NLSP in the MSSM. From these points of view, we do not pursue this possibility in this paper.

Finally, let us comment on models with a lighter gravitino. In our discussion, we have assumed that the gravitino is in the hundreds GeV to a few TeV range, where the NLSP decays outside of the detectors due to a limited size of $R$-parity violation as in Eq (8).
If the gravitino mass is a few tens of GeV, on the other hand, the bilinear $R$-parity violation terms can be as large as $\mu'/\mu \sim 10^{-7-8}$\textsuperscript{14}. In such cases, the NLSP lifetime can be as short as $\mathcal{O}(10^{-9})$ sec in the bi-linear $R$-parity violation\textsuperscript{21}. Thus, the neutral NLSP leaves a displaced vertex inside the detectors, and the charged NLSP leaves a kink inside the detectors\textsuperscript{15}. For such a light gravitino, however, the gravitino abundance requires $m_{\tilde{g}} \lesssim 500$ GeV which are severely constrained by the searches for multi-track displaced vertices for the neutral NLSP\textsuperscript{73,74} and by careful reinterpretation\textsuperscript{75} of the disappearing track searches for the charged NLSP\textsuperscript{76,77}. We leave detailed analysis for such a light gravitino for future work.

IV. CONCLUSIONS AND DISCUSSIONS

In this paper, we revisited the gravitino dark matter scenario in the presence of the bilinear $R$-parity violating interactions. In particular, we discussed the consistency with the thermal leptogenesis. For a high reheating temperature required for the thermal leptogenesis, the gravitino dark matter tends to be overproduced, which puts a severe upper limit on the gluino mass. As a result, we found that a large portion of parameter space has been excluded by the null results of the searches for multi-jets with missing momentum at the LHC experiments when the NLSP is assumed to be the neutralino. For the stau (and other charged slepton) NLSP, on the other hand, more stringent constraints are put by the searches for the long-lived charged particles at the LHC experiments. As a result, almost all the parameter space has been excluded unless the required reheating temperature is somewhat lowered by assuming, for example, a degenerated right-handed neutrino spectrum. For the colored NLSP candidates, constraints are tighter than the ones for the stau NLSP, and hence, the gravitino dark matter cannot be consistent with thermal leptogenesis in those cases, neither.

It should be noted that the constraints from cosmology are more stringent in the absence of the $R$-parity violation since the late-time decay of the NLSP contributes to the gravitino dark matter abundance\textsuperscript{55,57,58}. In addition, the properties of the NLSP\textsuperscript{14} for such a light gravitino, it mainly decays into a pair of a photon and a neutrino. The lifetime of such a gravitino is constrained to be $\tau_{3/2} \gtrsim 10^{29}$ sec by the searches for monochromatic gamma-ray line from the Galactic center region\textsuperscript{69}.

\textsuperscript{15} See e.g.\textsuperscript{70,72} for discussions on the short lived NLSP’s.
are also constrained very severely by the BBN due to a long lifetime of the NLSP in
the absence of $R$-parity violation. As a result, the successful BBN precludes the NLSP
candidates other than the charged sleptons or the sneutrinos \cite{55}. As for the charged
sleptons, however, the parameter region has been excluded by the LHC results as discussed
in this paper. The study of the sneutrino NLSP is a future work as mentioned above.

In our discussion, we focused on the bilinear $R$-parity violating interactions which
are expected to be dominant in wide range of models of spontaneous $R$-parity breaking
with the right-handed neutrinos \cite{16}. In fact, once $R$-parity is broken, the linear terms
of the right-handed neutrinos, $\varepsilon_{KR} N_R$, are generically allowed in the superpotential, which
leads to $\langle N \rangle_R \sim \varepsilon_{KR}/M_R$. Here, $\varepsilon_{KR}$ denotes an $R$-parity violating parameter and $M_R$ the
right-handed neutrino mass. Therefore, the resultant bilinear $R$-parity violating terms are
enhanced by $M_R^{-1}$ compared with trilinear $R$-parity violating terms which are suppressed
not by $M_R$ but by higher cutoff scales such as the Planck scale or the GUT scale depending
on the models.

Nontheless, when $R$-parity violation is dominated by trilinear terms \cite{17}, the gravitino
decays into three SM fermions at a tree-level and into a pair of a SM boson and a fermion
at the one loop level \cite{80, 81}. In those cases, the upper limits on the sizes of $R$-parity
violation from EGBR can be weaker than that in Eq. (8). Determination of the upper
limits on $R$-parity violation requires more careful analyses in those cases. If the constraints
can be relaxed to the ones in Eq. (2) \cite{18}, for example, the NLSP can decay promptly inside
the detectors, which relax the LHC constraints. We leave such studies for future work.

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\footnote{See e.g. discussion in \cite{78}.}
\footnote{See e.g. a model in \cite{79}.}
\footnote{Although this seems difficult unless the gravitino mass is below a few hundred GeV, which leads to a
severer upper limits on the gluino mass as in Fig. 1.}
Appendix A: A model of $R$-parity violation

1. $R$-parity violation tied with $U(1)_{B-L}$ breaking

In this appendix, we construct a model where the bilinear $R$-parity violating operators,

$$W = \mu'_{i} H_{u} L_{i},$$

appear in the range of Eq. (18) which are appropriate for the gravitino dark matter in the hundreds GeV to a TeV range. In particular, we consider a model where the $R$-parity violation is tied to a gauged $U(1)_{B-L}$ breaking as motivated in SO(10) GUT models [21, 22].

Here, we use the SO(10) GUT notation, although it is straightforward to decompose the following discussion in terms of the MSSM fields. In the SO(10) GUT models, the quarks and leptons are grouped into 16 representation, $16_{M}$, in conjunction with the right-handed neutrinos. The Higgs doublets are, on the other hand, grouped into 10 representation, $10_{H}$. In our discussion, we do not specify the mechanisms which explain the doublet-triplet splitting of the Higgs multiplets, and we assume that only the Higgs doublets in $10_{H}$ remain below the GUT scale.

In this notation, the MSSM Yukawa couplings are given by,

$$W_{\text{MSSM}} = 10_{H} 16_{M} 16_{M},$$

where we have suppressed the coefficient and the family indices for simplicity. To give a large Majorana masses to the right-handed neutrinos, we need to introduce bilinear terms of $16_{M}$, which require at least a VEV of 126 representation. However, an introduction of a field in the 126 representation leads to a blow up of the SO(10) gauge coupling constant just above the GUT scale. To avoid this problem, we instead break the $U(1)_{B-L} \subset SO(10)$
by a VEV of $\overline{16}_H$,

$$
\langle \overline{16}_H \rangle = v_{B-L} .
$$

(A3)

Here, as in the case of the Higgs doublets, we again assume that only the MSSM singlet in $\overline{16}_H$. With the VEV of $\overline{16}_H$, the Majorana mass terms are generated from,

$$
W_{N_R} = \frac{1}{2M_{PL}} \overline{16}_H \overline{16}_H 16_M 16_M .
$$

(A4)

It should be noted no $Z_2$ subgroup remains unbroken after $U(1)_{B-L}$ breaking.

For a later purpose, we assume that $v_{B-L} = O(10^{-(3-4)}) \times M_{PL}$, so that the right handed neutrino masses are in the range of

$$
M_R \sim \frac{1}{M_{PL}} v_{B-L}^2 \sim 10^{-(6-8)} \times M_{PL} .
$$

(A5)

Then, we aim to construct a model where the right-handed neutrinos obtain VEVs

$$
\langle N_R \rangle \simeq \frac{v_{B-L}^3}{M_{PL}^3} \times m_{3/2} ,
$$

(A6)

while the $R$-parity conserving $\mu$-term is given by $\mu \sim m_{3/2}$. Once these are achieved, we obtain an appropriate bilinear $R$-parity violating terms,

$$
\frac{\mu'}{\mu} \sim \frac{v_{B-L}^3}{M_{PL}^3} .
$$

(A7)

After the example of the model in [21], let us interconnect the $R$-parity violation to the $U(1)_{B-L}$ breaking scale. First, in order to give a VEV to $\overline{16}_H$, we consider a superpotential

$$
W = 10_H 16_M 16_M + \overline{16}_H \overline{16}_H 16_M 16_M + X (16_H \overline{16}_H - v_{B-L}^2) ,
$$

(A8)
where $16_H$ is a newly introduced $16$ representation and $X$ is an $SO(10)$ singlet. Hereafter, we take the unit of $M_{PL} = 1$. The first term of Eq. (A8) again denotes the MSSM Yukawa interaction, and the second term the Majorana mass term of the right-handed neutrinos. By the assumption of the split multiplet, $16_H$ and $\overline{16}_H$ contain the MSSM singlets only which are absorbed into $U(1)_{B-L}$ gauge multiplet once they obtain the vacuum expectation value.

In order to avoid too large $R$-parity violations, we forbid the following operators

$$W = 16_M \overline{16}_H ,$$
$$W = 10_H 16_M 16_H ,$$
$$W = 16_H 16_M 16_M 16_M .$$

(A9)

For that purpose, we consider a continuous $R$-symmetry broken by a spurion $v_{B-L}$ (see more discussions in the next subsection). In Tab. A1 we show the $R$-charge assignment which forbids the above operators.

A notable feature of the $R$-charge assignment in Tab. A1 is that it allows a Kähler potential,

$$K = v_{B-L}^4 16_M \overline{16}_H .$$

(A10)

which leads to a linear term of the right-handed neutrinos

$$W \sim m_{3/2} v_{B-L}^5 N_R .$$

(A11)

Thus, by combined with the Majorana mass term, the right-handed neutrinos obtain VEVs,

$$\langle N_R \rangle \simeq v_{B-L}^3 \times m_{3/2} .$$

(A12)

which generate the bilinear $R$-parity violation through the first term of Eq. (A8),

$$\mu' = v_{B-L}^3 m_{3/2} .$$

(A13)

---

19 If we regard $m_{3/2}$, we may directly write down this term.
| $\mathbf{16}$ | $\mathbf{10}$ | $\mathbf{16}$ | $\mathbf{\bar{16}}$ | $Q$ | $\bar{Q}$ | $X$ |
|---|---|---|---|---|---|---|
| $R$ | 1 | 0 | $-1/2$ | 0 | $-1/4$ | $-1/4$ | $5/2$ |
| $\mathbb{Z}_{10}$ | $-4$ | 0 | 2 | 0 | 1 | 1 | 0 |

TABLE II. $R$-charges of matter fields, Higgs fields and SO(10) singlets. We also show the charge assignment of $\mathbb{Z}_{10}$ with which the terms with charges $-8 \pmod{10}$ are allowed in the superpotential.

The $R$-symmetric $\mu$-term is, on the other hand, given by

$$W \sim m_{3/2} \mathbf{10}_H \mathbf{10}_H \ . \ (A14)$$

Therefore, we find that the bilinear $R$-parity violation are given by\(^{20}\)

$$\frac{\mu'}{\mu} \sim v_{B-L}^3 \ . \ (A15)$$

2. Model with discrete $R$-symmetry

In the above example, we made use of a continuous $R$-symmetry which is broken by the spurion $v_{B-L}$. In this subsection, we discuss a model where $v_{B-L}$ is dynamical. For that purpose, we consider $SU(5)$ gauge theory with four-flavor of vector-like pairs of fundamental representation $(Q, \bar{Q})$, and replace $v_{B-L}^2$ to a composite operator $(Q\bar{Q})$. Then, the superpotential in Eq. (A8) is rewritten by,

$$W = \mathbf{10}_H \mathbf{16}_M \mathbf{16}_M + \mathbf{\bar{16}}_H \mathbf{\bar{16}}_H \mathbf{16}_M \mathbf{16}_M + X(\mathbf{16}_H \mathbf{\bar{16}}_H - Q\bar{Q}) \ , \ (A16)$$

where the $R$-charge assignment is given in Tab. A2\(^{21}\). Since the $SU(5)$ gauge theory with four-flavor does not have a vacuum, we add explicit mass terms

$$W = \mathbf{10}_H \mathbf{16}_M \mathbf{16}_M + \mathbf{\bar{16}}_H \mathbf{\bar{16}}_H \mathbf{16}_M \mathbf{16}_M + X(\mathbf{16}_H \mathbf{\bar{16}}_H - Q\bar{Q}) + m_{Q\bar{Q}}^\prime \ . \ (A17)$$

---

\(^{20}\) The actual $R$-parity violating bilinear terms are multiplied by the neutrino Yukawa couplings.

\(^{21}\) This charge assignment is free from the $SU(5)$ anomaly.
With the explicit mass term, the $R$-symmetry is explicitly broken down to a discrete $\mathbb{Z}_{10R}$ symmetry whose charge assignment is given in the second line of Tab. A2.\footnote{As we will see, we require $m_Q \ll 1$. For that purpose, we assume that $m_Q, X, 16_H$ and $Q\bar{Q}$ are charged under some additional discrete symmetry.}

Below the dynamical scale of $SU(5)$, non-perturbative potential is generated \footnote{L. J. Hall and M. Suzuki, Nucl. Phys. B231, 419 (1984)}

\[
W = 10_H 16_M 16_M + 16_H 16_H 16_M 16_M + X(16_H 16_H - Q\bar{Q}) + m_Q Q\bar{Q} + \frac{\Lambda^{11}}{\det Q\bar{Q}},
\]

where $\Lambda$ denotes the dynamical scale of $SU(5)$. As a result, $Q\bar{Q}$ obtains a VEV, which provides the spurion in the previous section

\[
v_{B-L}^2 \sim \langle Q\bar{Q} \rangle \sim \left(\frac{\Lambda^{11}}{m_Q}\right)^{1/5}.
\]

Thus, by arranging

\[
\left(\frac{\Lambda^{11}}{m_Q}\right)^{1/5} = O(10^{-6}),
\]

we can provide an appropriate spurion $v_{B-L} = O(10^{-3})$. Furthermore, we can also provide an appropriate size of the graviton mass by taking

\[
m_Q \simeq 10^{-9}, \quad \Lambda \simeq 10^{-3.5},
\]

which leads to an appropriate VEV of the superpotential simultaneously

\[
m_{3/2} = \langle W \rangle \sim m_Q \langle Q\bar{Q} \rangle \simeq 10^{-15}.
\]
[4] G. V. Lavrelashvili, V. A. Rubakov, and P. G. Tinyakov, JETP Lett. 46, 167 (1987), [Pisma Zh. Eksp. Teor. Fiz.46,134(1987)].

[5] S. B. Giddings and A. Strominger, Nucl. Phys. B307, 854 (1988).

[6] S. R. Coleman, Nucl. Phys. B310, 643 (1988).

[7] G. Gilbert, Nucl. Phys. B328, 159 (1989).

[8] T. Banks and N. Seiberg, Phys. Rev. D83, 084019 (2011) arXiv:1011.5120 [hep-th].

[9] L. M. Krauss and F. Wilczek, Phys. Rev. Lett. 62, 1221 (1989).

[10] J. Preskill and L. M. Krauss, Nucl. Phys. B341, 50 (1990).

[11] J. Preskill, S. P. Trivedi, F. Wilczek, and M. B. Wise, Nucl. Phys. B363, 207 (1991).

[12] T. Banks and M. Dine, Phys. Rev. D45, 1424 (1992) arXiv:hep-th/9109045 [hep-th].

[13] S. Dimopoulos and H. Georgi, Nucl. Phys. B193, 150 (1981).

[14] S. Weinberg, Phys. Rev. D26, 287 (1982).

[15] N. Sakai and T. Yanagida, Nucl. Phys. B197, 533 (1982).

[16] S. Dimopoulos, S. Raby, and F. Wilczek, Phys. Lett. B112, 133 (1982).

[17] T. Yanagida, Proceedings: Workshop on the Unified Theories and the Baryon Number in the Universe: Tsukuba, Japan, February 13-14, 1979, Conf. Proc. C7902131, 95 (1979).

[18] P. Ramond, in International Symposium on Fundamentals of Quantum Theory and Quantum Field Theory Palm Coast, Florida, February 25-March 2, 1979 (1979) pp. 265–280, arXiv:hep-ph/9809459 [hep-ph].

[19] P. Minkowski, Phys. Lett. B67, 421 (1977).

[20] T. Watari, JHEP 11, 065 (2015) arXiv:1506.08433 [hep-th].

[21] W. Buchmuller, L. Covi, K. Hamaguchi, A. Ibarra, and T. Yanagida, JHEP 03, 037 (2007) arXiv:hep-ph/0702184 [HEP-PH].

[22] J. Schmidt, C. Weniger, and T. T. Yanagida, Phys. Rev. D82, 103517 (2010) arXiv:1008.0398 [hep-ph].

[23] F. Takayama and M. Yamaguchi, Phys. Lett. B485, 388 (2000) arXiv:hep-ph/0005214 [hep-ph].

[24] G. Moreau and M. Chemtob, Phys. Rev. D65, 024033 (2002) arXiv:hep-ph/0107286 [hep-ph]
[25] M. Fukugita and T. Yanagida, Phys. Lett. **B174**, 45 (1986).
[26] G. F. Giudice, A. Notari, M. Raidal, A. Riotto, and A. Strumia, Nucl. Phys. **B685**, 89 (2004), arXiv:hep-ph/0310123 [hep-ph].
[27] W. Buchmuller, R. D. Peccei, and T. Yanagida, Ann. Rev. Nucl. Part. Sci. **55**, 311 (2005), arXiv:hep-ph/0502169 [hep-ph].
[28] S. Davidson, E. Nardi, and Y. Nir, Phys. Rept. **466**, 105 (2008), arXiv:0802.2962 [hep-ph].
[29] M. Bolz, A. Brandenburg, and W. Buchmuller, Nucl. Phys. **B606**, 518 (2001), Erratum: Nucl. Phys.B790,336(2008), arXiv:hep-ph/0012052 [hep-ph].
[30] K. Hamaguchi, F. Takahashi, and T. T. Yanagida, Phys. Lett. **B677**, 59 (2009), arXiv:0901.2168 [hep-ph].
[31] R. Barbier et al., Phys. Rept. **420**, 1 (2005), arXiv:hep-ph/0406039 [hep-ph].
[32] T. Christodoulakis and E. Korfiatis, Phys. Lett. **B256**, 457 (1991).
[33] W. Fischler, G. F. Giudice, R. G. Leigh, and S. Paban, Phys. Lett. **B258**, 45 (1991).
[34] H. K. Dreiner and G. G. Ross, Nucl. Phys. **B410**, 188 (1993), arXiv:hep-ph/9207221 [hep-ph].
[35] M. Endo, K. Hamaguchi, and S. Iwamoto, JCAP **1002**, 032 (2010), arXiv:0912.0585 [hep-ph].
[36] T. Higaki, K. Nakayama, K. Saikawa, T. Takahashi, and M. Yamaguchi, Phys. Rev. **D90**, 045001 (2014), arXiv:1404.5796 [hep-ph].
[37] I. Affleck and M. Dine, Nucl. Phys. **B249**, 361 (1985).
[38] M. Dine, L. Randall, and S. D. Thomas, Nucl. Phys. **B458**, 291 (1996), arXiv:hep-ph/9507453 [hep-ph].
[39] E. Giusarma, M. Gerbino, O. Mena, S. Vagnozzi, S. Ho, and K. Freese, (2016), arXiv:1605.04320 [astro-ph.CO].
[40] M. Ibe, S. Iwamoto, S. Matsumoto, T. Moroi, and N. Yokozaki, JHEP **08**, 029 (2013), arXiv:1304.1483 [hep-ph].
[41] K. Ishiwata, S. Matsumoto, and T. Moroi, Phys. Rev. **D78**, 063505 (2008), arXiv:0805.1133
[hep-ph] Phys. Lett. B675, 446 (2009), arXiv:0811.0250 [hep-ph]; JHEP 05, 110 (2009), arXiv:0903.0242 [hep-ph].

[42] T. Delahaye and M. Grefe, JCAP 1312, 045 (2013), arXiv:1305.7183 [hep-ph].

[43] A. Ibarra and D. Tran, Phys. Rev. Lett. 100, 061301 (2008), arXiv:0709.4593 [astro-ph].

[44] K. Ishiwata, S. Matsumoto, and T. Moroi, Phys. Lett. B679, 1 (2009), arXiv:0905.4593 [astro-ph.CO].

[45] E. Carquin, M. A. Diaz, G. A. Gomez-Vargas, B. Panes, and N. Viaux, Phys. Dark Univ. 11, 1 (2016), arXiv:1501.05932 [hep-ph].

[46] S. Ando and K. Ishiwata, JCAP 1505, 024 (2015), arXiv:1502.02007 [astro-ph.CO]; JCAP 1606, 045 (2016), arXiv:1604.02263 [hep-ph].

[47] L. Covi, M. Grefe, A. Ibarra, and D. Tran, JCAP 0901, 029 (2009), arXiv:0809.5030 [hep-ph].

[48] M. Ackermann et al. (Fermi-LAT), Astrophys. J. 799, 86 (2015), arXiv:1410.3696 [astro-ph.HE].

[49] V. S. Rychkov and A. Strumia, Phys. Rev. D75, 075011 (2007), arXiv:hep-ph/0701104 [hep-ph].

[50] J. Ellis, M. A. G. Garcia, D. V. Nanopoulos, K. A. Olive, and M. Peloso, JCAP 1603, 008 (2016), arXiv:1512.05701 [astro-ph.CO].

[51] J. Pradler and F. D. Steffen, Phys. Rev. D75, 023509 (2007), arXiv:hep-ph/0608344 [hep-ph].

[52] S. Antusch and A. M. Teixeira, JCAP 0702, 024 (2007), arXiv:hep-ph/0611232 [hep-ph].

[53] P. A. R. Ade et al. (Planck), (2015), arXiv:1502.02114 [astro-ph.CO].

[54] J. L. Feng, A. Rajaraman, and F. Takayama, Phys. Rev. Lett. 91, 011302 (2003), arXiv:hep-ph/0302215 [hep-ph]; Phys. Rev. D68, 063504 (2003), arXiv:hep-ph/0306024 [hep-ph].

[55] M. Fujii, M. Ibe, and T. Yanagida, Phys. Lett. B579, 6 (2004), arXiv:hep-ph/0310142 [hep-ph].

[56] J. L. Feng, S.-f. Su, and F. Takayama, Phys. Rev. D70, 063514 (2004), arXiv:hep-ph/0404198 [hep-ph]; J. L. Feng, S. Su, and F. Takayama, Phys. Rev. D70, 075019
[57] J. Heisig, JCAP 1404, 023 (2014), arXiv:1310.6352 [hep-ph].

[58] A. Arbey, M. Battaglia, L. Covi, J. Hasenkamp, and F. Mahmoudi, Phys. Rev. D92, 115008 (2015) arXiv:1505.04595 [hep-ph].

[59] M. Kawasaki, K. Kohri, and T. Moroi, Phys. Rev. D71, 083502 (2005), arXiv:astro-ph/0408426 [astro-ph].

[60] K. Jedamzik, Phys. Rev. D74, 103509 (2006), arXiv:hep-ph/0604251 [hep-ph].

[61] M. Hirsch, W. Porod, and D. Restrepo, JHEP 03, 062 (2005), arXiv:hep-ph/0503059 [hep-ph].

[62] ATLAS collaboration, ATLAS-CONF-2016-078 (2016).

[63] CMS Collaboration, CMS-PAS-EXO-15-010 (2015).

[64] C. Borschensky, M. Krämer, A. Kulesza, M. Mangano, S. Padhi, T. Plehn, and X. Portell, Eur. Phys. J. C74, 3174 (2014), arXiv:1407.5066 [hep-ph].

[65] CMS Collaboration, CMS-PAS-SUS-16-014 (2016).

[66] T. Cohen, T. Golling, M. Hance, A. Henrichs, K. Howe, J. Loyal, S. Padhi, and J. G. Wacker, in Proceedings, Community Summer Study 2013: Snowmass on the Mississippi (CSS2013): Minneapolis, MN, USA, July 29-August 6, 2013 (2013) arXiv:1310.0077 [hep-ph].

[67] G. R. Farrar, Supersymmetry in physics. Proceedings, 5th International Conference, SUSY’97, Philadelphia, USA, May 27-31, 1997, Nucl. Phys. Proc. Suppl. 62, 485 (1998), arXiv:hep-ph/9710277 [hep-ph].

[68] A. C. Kraan, J. B. Hansen, and P. Nevski, Eur. Phys. J. C49, 623 (2007), arXiv:hep-ex/0511014 [hep-ex].

[69] M. Ackermann et al. (Fermi-LAT), Phys. Rev. D91, 122002 (2015) arXiv:1506.00013 [astro-ph.HE].

[70] S. Asai, Y. Azuma, M. Endo, K. Hamaguchi, and S. Iwamoto, JHEP 12, 041 (2011), arXiv:1103.1881 [hep-ph].

[71] P. W. Graham, D. E. Kaplan, S. Rajendran, and P. Saraswat, JHEP 07, 149 (2012).
[72] C. Csaki, E. Kuflik, S. Lombardo, O. Slone, and T. Volansky, JHEP 08, 016 (2015), arXiv:1505.00784 [hep-ph].

[73] The ATLAS collaboration, ATLAS-CONF-2013-092 (2013).

[74] G. Aad et al. (ATLAS), Phys. Rev. D92, 072004 (2015) arXiv:1504.05162 [hep-ex].

[75] J. A. Evans and J. Shelton, JHEP 04, 056 (2016) arXiv:1601.01326 [hep-ph].

[76] G. Aad et al. (ATLAS), Phys. Rev. D88, 112006 (2013) arXiv:1310.3675 [hep-ex].

[77] V. Khachatryan et al. (CMS), JHEP 01, 096 (2015) arXiv:1411.6006 [hep-ex].

[78] S. Shirai, F. Takahashi, and T. T. Yanagida, Phys. Lett. B680, 485 (2009), arXiv:0905.0388 [hep-ph].

[79] B. Bhattacherjee, J. L. Evans, M. Ibe, S. Matsumoto, and T. T. Yanagida, Phys. Rev. D87, 115002 (2013) arXiv:1301.2336 [hep-ph].

[80] N. E. Bomark, S. Lola, P. Osland, and A. R. Raklev, Phys. Lett. B677, 62 (2009) arXiv:0811.2969 [hep-ph].

[81] N. E. Bomark, S. Lola, P. Osland, and A. R. Raklev, Phys. Lett. B686, 152 (2010) arXiv:0911.3376 [hep-ph].

[82] I. Affleck, M. Dine, and N. Seiberg, Nucl. Phys. B241, 493 (1984).