Self-Supervised Pyramid Representation Learning
for Multi-Label Visual Analysis and Beyond

Supplementary Material

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A. Pseudocode of SS-PRL

We provide the pseudocode of our proposed Self-Supervised Pyramid Representation Learning (SS-PRL) in Algorithm 1.

B. Implementation Details

Implementation Details of SS-PRL. We conduct all experiments by training 200 epochs with a batch size of 128 on MSCOCO [10] or 100 epochs with a batch size of 256 on ImageNet [3]. We use Resnet-50 [8] as our backbone network. The projection head for each scale is a 2-layer multi-layer perceptron (MLP) head that embeds the pyramid representations into a 128-dim space (D = 128). We use single linear layers as the cross-scale correlation learners (Section 3.2.2). The number of prototypes K0, K1 and K2 are set to 300, 150, and 150, respectively. The temperature parameter τ in Equation (4) is set as 1.0. We set αs (Equation (2)) as 1.0 for s = 0 and 0.25 for other scales, and βs (Equation (3)) is selected as the same values as αs for simplicity. We adopt the same optimization method as in [1]. We use a weight decay of 10^{-6}, LARS optimizer [20] with an initial learning rate of 0.6, and the cosine learning rate decay with a final value of 0.0006.

Data Augmentations. Unless specified, we construct pyramid views consisting of 3 different spatial scales (i.e., s = 0, 1, 2). The image patch groups V0, V1 and V2 contain 1, 4, and 9 non-overlapping augmented patches, respectively. Our image patch groups are generated as follows: First, a random region is cropped with at least 14%, 60%, 60% of the original image and then resized to 224 × 224, 314 × 314, and 383 × 383 for s = 0, 1, 2. We directly use the 224 × 224 image as the single patch in V0, i.e., at the global image level. To generate V1 consisting of 4 patches (M1 = 4), we resize the image to 314 × 314, divide it into 2 × 2 grids, and then apply the random crop on each grid to get patches of size 112 × 112; to generate V2 containing 9 patches (M2 = 9), we divide the 383 × 383 resized image into 3 × 3 grids and then apply the random crop on each grid to get patches of size 96 × 96. Finally, all the patches are applied with the same set of image augmentation, which includes random horizontal flip, color jittering, gray-scale conversion, and Gaussian blur, following the same implementation as [2, 6, 1].

Implementation Details of Downstream Multi-Label Classification with Fine-tuned Linear Classifiers. We train a linear multi-label classifier on top of the fixed pre-trained backbone network (i.e., ResNet-50) on COCO train2014 [10] and VOC trainval07 [4], and then report mean average precision (mAP) on COCO val2014 [10] and VOC test2007 [4]. All images are first resized to 256 pixels along the shorter side, and then center-cropped to 224 × 224. We train the linear classifier using stochastic gradient decent for 50 epochs with weight decay of 0.0001, momentum of 0.9, and a batch size of 32/128 on VOC [4]/COCO [10]. Grid search of range [0.001, 3.0] is applied to the initial learning rate of each linear classifier pre-trained with different method. The learning rate reduces by a factor of 10 three times (equally spaced intervals).

Implementation Details of Downstream Multi-Label Classification in Semi-Supervised Settings. We fine-tune the whole network with 1%, 10%, and 100% labeled data from COCO train2014 [10] and report mAP on COCO val2014 [10]. The network is fine-tuned for 20 epochs with a batch size of 128 when using 1% labeled data and a batch size of 32 when using 10% or 100% labeled data. We use grid search within the range of [0.001, 0.1] to set distinct learning rates for the backbone network and the final linear layer, and we decay the learning rates by 0.2 at the 12th and 16th epochs. Other hyperparameters are kept the same as in the linear evaluation setting, i.e., fine-tuned

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We use the 1-shot ranking and Instance Segmentation. Implementation Details of Downstream Object Detection. We report the result of detector with backbone, FPN [9] and prediction heads during the training [16, 15], synchronized batch normalization is applied in each epoch with a batch size of 128 or on ImageNet [3] with a batch size of 256.

**Algorithm 1:** Self-Supervised Pyramid Representation Learning (SS-PRL)

**Input:** feature extractor \( f_\theta \), cross-scale correlation learners \( g_\phi = \{g_{\phi,s}\}_{s=1}^S \), multi-level semantic prototypes \( \{C_s\}_{s=0}^S \), batch size \( B \), temperature \( \tau \), weights of loss terms \( \{\alpha_s\}_{s=0}^S \), \( \{\beta_s\}_{s=1}^S \), and \( \lambda \)

**Data:** unlabeled dataset \( D_u \)

**Output:** backbone network \( f_\theta \)

```python
for sampled minibatch \( x \) do
  for \( s \) in \( 0 : S \) do
    generate \( \mathbf{V}_s \) and \( \mathbf{V}'_s \) from \( x \)
    \( Z_s, Z'_s = f_\theta(V_s), f_\theta(V'_s) \# (B \times M_s, D) \)
    \( Q_s, Q'_s = S-K(Z_s, C_s), S-K(Z'_s, C_s) \# (B \times M_s, K_s) \)
    \( P_s, P'_s = \text{softmax}(\frac{1}{2}Z_sC_s), \text{softmax}(\frac{1}{2}Z'_sC_s) \# (B \times M_s, K_s) \)
  end
  \# loss function
  \( L_{pyr} = -\sum_s \alpha_s \text{mean}(Q_s \log P'_s + Q'_s \log P_s) \)
  \( L_{cross} = -\sum_{s \neq 0} \beta_s \text{mean}(Q_0 \log g_{\phi,s}(\text{Avg}(P_s)) + Q'_0 \log g_{\phi,s}(\text{Avg}(P'_s))) \)
  \( L = L_{pyr} + \lambda L_{cross} \)
  \# optimization step
  update \( f_\theta, g_\phi \), and \( \{C_s\}_{s=0}^S \) to minimize \( L \)
  normalize \( \{C_s\}_{s=0}^S \)
end
```

**Implementation Details of Downstream Object Detection and Instance Segmentation.** We use the 1× schedule in Detectron2 [17] to fine-tune a Mask R-CNN [7] detector with FPN [9] backbone (pre-trained with each self-supervised method) on COCO train2014 [10] and evaluate on COCO val2014 [10]. Following the settings in [16, 15], synchronized batch normalization is applied in backbone, FPN [9] and prediction heads during the training. We report the result of detector with 15k training iterations to compare the transfer ability of each SSL pre-training method.

**C. Further Quantitative Comparisons**

In this section, we provide further quantitative comparisons of our SS-PRL against existing SSL methods on downstream semantic segmentation tasks. We also conduct experiments to verify the effectiveness of visual pre-training with SS-PRL on downstream state-of-the-art multi-label classification methods. For fair comparisons, all models are pre-trained on COCO train2014 [10] for 200 epochs with a batch size of 128 or on ImageNet [3] with a batch size of 256.

**Downstream Semantic Segmentation on PASCAL VOC.** We provide comparisons with previous SSL methods using the downstream semantic segmentation task on PASCAL VOC [4] to further exhibit the effectiveness and robustness of our SS-PRL. We report the mIoU using an FCN backbone network [11] fine-tuned on VOC train_aug2012 set (10582 images) [4] for 20k iterations and then evaluated on val2012 set [4]. We mostly follow the same settings as [16], where the first 7 × 7 convolution is kept, the batch size is set to 16, and the crop size is selected as 512, except the learning rate is set to 0.05. As shown in Table S-A, SS-PRL outperforms most SSL methods by achieving 62.6% mIoU and even exceeds SSL methods that are specifically designed for dense prediction tasks [18, 21, 19].

**Transfer to SOTA Multi-Label Classification Methods.** To examine the impact of visual pre-training with SS-PRL on downstream state-of-the-art methods, we further provide results by fine-tuning the pre-trained backbone network on COCO train2014 [10] with the asymmetric loss [13]. Following the settings in [13], we train the model with Adam optimizer and 1-cycle policy [14], with a maximal
Table S-A. **Downstream semantic segmentation task on the PASCAL VOC dataset.** We report the mean IoU (mIoU) on VOC with fine-tuned FCN models. All methods are pre-trained on COCO for 200 epochs. Top-3 best pre-training methods are underlined.

| Method            | Semantic Segmentation on VOC (mIoU) |
|-------------------|-------------------------------------|
| Random Init.      | 40.7                                |
| MoCo v2 [6]       |                                     |
| SwAV [1]          | 57.3                                |
| BYOL [5]          | 56.1                                |
| DenseCL [16]      | 54.1                                |
| DetCo [18]        |                                     |
| MaskCo [21]       |                                     |
| InsLoc [19]       |                                     |
| **SS-PRL (ours)** | 62.6                                |

Table S-B. **Transfer to a SOTA multi-label classification method.** We report the mAP on COCO with the whole network fine-tuned with asymmetric loss [13] for 40 epochs. All methods are pre-trained on COCO with 200 epochs or ImageNet with 100 epochs, respectively.

| Method            | Multi-Label Classification with ASL [13] on COCO (mAP) |
|-------------------|-------------------------------------------------------|
| Random Init.      | Pretrained on COCO: 50.0                               |
|                   | Pretrained on ImageNet: 50.0                           |
| MoCo v2 [6]       | General-purpose: 63.8                                  |
| SwAV [1]          |                                                      |
| BYOL [5]          |                                                      |
| DenseCL [16]      | Dense prediction: 68.7                                 |
| DetCo [18]        |                                                      |
| MaskCo [21]       |                                                      |
| InsLoc [19]       |                                                      |
| **SS-PRL (ours)** | 69.3 (Pretrained on COCO)                            |
|                   | 73.8 (Pretrained on ImageNet)                         |

learning rate of 2e-4. All the models are fine-tuned for 40 epochs. Note that we use ResNet-50 as our backbone instead of TResNet-L as used in [13]. As shown in Table S-B, SS-PRL again outperforms other SSL methods with 69.3 % mAP when pre-trained on COCO and 73.8 % mAP when pre-trained on ImageNet. The experiment demonstrates the effectiveness of SS-PRL in downstream multi-label image classification, even when applied to state-of-the-art methods.

**D. More Visualization Results**

Prototypes learned at each scale. Figure A1 visualizes the semantic concepts portrayed by our learned prototypes at different patch levels on the COCO dataset [10]. We observe that prototypes at scale 0 tend to encapsulate the concept of entire scenes that include multiple objects or items (e.g., motorcycle with a rider or steam train blowing smoke), while prototypes at scale 1 tend to capture a single object in an image (e.g., a motorcycle or a train), and prototypes at scale 2 tend to portray a fine-grained item (e.g., a tire or rail).

It shows that SS-PRL is able to discover the hierarchical semantic structure of the dataset with our proposed pyramid representation learning.

**E. Further Analysis**

For the completeness of analysis, we conduct further experiments by training SS-PRL with two spatial scales (i.e., \(s = 0, 1\)). SS-PRL trained with a single spatial scale (i.e., \(s = 0\)) is adopted as the baseline. All the implementation details follow the settings introduced in Section B, except that here we set the number of prototypes \(K_1\) as 300, the weights of loss terms \(\alpha_1\) and \(\beta_1\) as 0.5.

**Further Discussion on Patch-Level Semantic Prototypes.** In Table S-C, we report the linear evaluation [12] results of SS-PRL with semantic prototypes \(C_s\) trained under different scenarios. Similar to Table 4 in our main paper, we observe that SS-PRL still achieves the best performance when distinct sets of prototypes are applied in different spatial scales, indicating that exploring the hierarchical infor-
Figure A1. Visual concepts captured by the learned prototypes at each scale on COCO. Each column shows example images/patches associated with the learned prototypes (in each sub-column) at the corresponding patch scale. Our SS-PRL is shown to exploit hierarchical semantic information from image data by learning patch-level prototypes with semantic practicality (e.g., scenes with motorcycles at scale 0, motorcycle at scale 1, and tires at scale 2).

### Table S-C. Ablation Studies on the derived patch-level prototypes with two spatial scales ($s = 0, 1$). Note that Shared across all scales indicates the same prototypes learned across patch scales (i.e., same $C_s$ at different patch scales in Fig. 1). Similar to the results in Table 4, we see that prototypes learned from each scale enforced by our cross-scale correlation would be desirable.

| Prototype                        | mAP  |
|----------------------------------|------|
| Baseline                         | 79.2 |
| Shared across all scales         | 77.8 |
| Learned & correlated across scales | **79.9** |

### Table S-D. Ablation: Impact of the number of semantic prototypes $K_s$ for multi-label classification on VOC dataset.

With the feature extractor learned and frozen with different supervised/self-supervised methods, we report the mAP on VOC with fine-tuned linear classifiers. The model shows the best results when trained with comparable $K_0$ and $K_1$.

| # of Prototypes | Scale 0 ($K_0$) | Scale 1 ($K_1$) | mAP  |
|-----------------|-----------------|-----------------|------|
| 3000            | 1500            | 77.6            |
| 300             | 1500            | 79.6            |
| 300             | 300             | 79.9            |
| 300             | 15              | 79.9            |
| 300             | 0               | 79.2            |

Parameter Analysis. In Table S-D, we evaluate the influence of the number of semantic prototypes utilized at two spatial scales by reporting the multi-label classification mAP on VOC [4]. Here we only adopt two image scales (i.e., $s = 0, 1$) for network training to better understand the relationships between $K_s$ from two different spatial scales. The results show that the performance greatly degrades when the number of prototypes at the global image level $K_0$ is selected as a large number (3000). It indicates that $K_0$ should not be varied considerably from the actual number of labels (80) of the training dataset (i.e. COCO [10]), since a large $K_0$ easily leads to over-clustering or redundant information. We also experiment with different numbers of patch-level prototypes (e.g. scale 1 $K_1$) with a fixed $K_0$ (300). As $K_1$ increases from 0 to 300, the performance improves from 79.2 % to 79.9 % mAP. This suggests that the exploitation of fine-grained information from patches indeed facilitates the downstream multi-label classification task. Note that the performance converges and even degrades when $K_1$ increases from 150 to 1500. The sweet point in the observed reverse U-shape of performance lies at $K_1 = K_0 = 300$, indicating the number of prototypes chosen at each spatial scale should be comparable.
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