Updated Cross Section Measurement of $e^+e^- \rightarrow K^+K^- J/\psi$ and $K_S^0 K_S^0 J/\psi$ via Initial State Radiation at Belle

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Abstract

The cross sections of the processes $e^+e^- \rightarrow K^+K^-J/\psi$ and $K^0_S K^0_S J/\psi$ are measured via initial state radiation at center-of-mass energies between the threshold and 6.0 GeV using a data sample of 980 fb$^{-1}$ collected with the Belle detector on or near the $\Upsilon(nS)$ resonances, where $n = 1, 2, ..., 5$. The cross sections for $e^+e^- \rightarrow K^+K^-J/\psi$ are at a few pb level and the average cross section for $e^+e^- \rightarrow K^0_S K^0_S J/\psi$ is $1.8 \pm 0.6\text{(stat.)} \pm 0.3\text{(syst.)}$ pb between 4.4 and 5.2 GeV. All of them are consistent with previously published results with improved precision. A search for resonant structures and associated intermediate states in the cross section of the process $e^+e^- \rightarrow K^+K^-J/\psi$ is performed.

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I. INTRODUCTION

Recently a new charged charmoniumlike state, the \(Z(3900)\), was observed by the Belle \[1\] and BESIII \[2\] experiments in a study of \(e^+e^- \rightarrow \pi^+\pi^- J/\psi\) at center-of-mass (CM) energies around 4.26 GeV. It was soon confirmed with the CLEO data at a CM energy of 4.17 GeV \[3\]. As the \(Z(3900)\) state has a strong coupling to charmonium and is charged, it cannot be a conventional charmonium state. This observation has stimulated a number of distinct interpretations. These include a tetraquark state \[4\], \(DD^*\) molecule \[5\], hadroquarkonium \[6\], and other configurations \[7\]. More recently, BESIII observed another charged charmoniumlike state, \(Z_c(4020)\), in \(e^+e^- \rightarrow \pi^+\pi^- J/\psi\) \[8\]. These states, together with similar states observed in the bottomonium system \[9\], indicate the existence of a new class of hadrons.

A strange partner of the \(Z(3900)\), called \(Z_{c\bar{s}}\), may exist in the above scenarios. The mass of a \(J^P = 1^+ D_s\bar{D}^*\) molecular state was first predicted \[10\] using QCD sum rules with \(M(Z_{c\bar{s}}) = (3.97 \pm 0.08)\) GeV/\(c^2\), which is very close to the \(D_s^+\bar{D}^{*0}\) threshold of 3.976 GeV/\(c^2\). Using the same QCD sum rules, the authors of Ref. \[11\] calculated the decay widths of the \(Z_{c\bar{s}}\) to \(K^+J/\psi\), \(K^+\eta_c\), \(D_s^+\bar{D}^{*0}\) and \(\bar{D}^0D_s^{*+}\), assuming the \(Z_{c\bar{s}}\) to be a tetraquark state. Such a state is also predicted in the single-kaon emission model \[12\].

Using a data sample of 673 fb\(^{-1}\) collected at or near \(\sqrt{s} = 10.58\) GeV, Belle has observed abundant \(e^+e^- \rightarrow K^+K^- J/\psi\) signal events via initial state radiation (ISR) \[13\]. In addition, there is one very broad structure in the \(K^+K^- J/\psi\) mass spectrum; fits using either a single Breit-Wigner (BW) function, or the \(\psi(4415)\) plus a second BW function yield resonant parameters that are very different from those of the currently tabulated excited \(\psi\) states \[14\]. Unfortunately, the \(M(K^\pm J/\psi)\) distribution is not shown in Ref. \[13\].

In this paper, we report the updated measurement of the cross sections for \(e^+e^- \rightarrow K^+K^- J/\psi\) and \(K_{s0}^0K_{S0}^0 J/\psi\) between threshold and 6.0 GeV/\(c^2\) and examine possible resonant structures in the cross section of the process \(e^+e^- \rightarrow K^+K^- J/\psi\) as well as in the \(K^\pm J/\psi\) and \(K^+K^-\) systems. The results are based on the full Belle data sample with an integrated luminosity of 980 fb\(^{-1}\) collected on or near the \(Y(nS)\) \((n = 1, 2, ..., 5)\).

The Belle detector at the KEKB asymmetric-energy \(e^+e^-\) collider \[15\] is described in detail elsewhere \[16\]. This analysis supersedes that reported in Ref. \[13\] where a subset of the Belle data sample was used.

We use the PHOKHARA \[17\] program to generate signal Monte Carlo (MC) events and determine experimental efficiencies. In the generator, one or two photons are allowed to be emitted before forming the resonance \(X\); then \(X\) decays into \(K^+K^- J/\psi\) with \(J/\psi\) decaying into \(\ell^+\ell^-\) \((\ell = e, \mu)\). When generating the MC sample, the mass of \(X\) is fixed to a certain value while the width is set to zero. In \(X \rightarrow K^+K^- J/\psi\), a pure \(S\)-wave between the \(K^+K^-\) system and the \(J/\psi\) as well as between the \(K^+\) and \(K^-\) is assumed. The invariant mass of the \(K^+K^-\) system is generated uniformly in phase space. To estimate the model uncertainty, we also generate events with a \(K^+K^-\) invariant mass distributed like \(M(\pi^+\pi^-)\) in \(\psi(2S) \rightarrow \pi^+\pi^- J/\psi\) decays \[18\].

II. EVENT SELECTION

The selection of \(K^+K^-\ell^+\ell^-\) events is the same as in Ref. \[13\]. For the events of interest, we require four well reconstructed charged tracks with zero net charge. The impact parameters of
these tracks perpendicular to and along the beam direction with respect to the interaction point are required to be less than 0.5 cm and 4.0 cm, respectively. For each charged track, a combined likelihood ratio from various detector subsystems is formed to identify different particle species \((e, \mu, \pi, K, p)\). Tracks with \(\mathcal{R}_K = \frac{L_K}{L_K + L_{\pi}} > 0.6\) are identified as kaons with an efficiency of about 92%; about 4% are misidentified pions [19]. Similar ratios are also defined for leptons [20, 21].

For electrons from \(J/\psi \rightarrow e^+ e^-\), one track should have \(\mathcal{R}_e > 0.95\) and the other \(\mathcal{R}_\mu > 0.05\); for muons from \(J/\psi \rightarrow \mu^+ \mu^-\), at least one track should have \(\mathcal{R}_\mu > 0.95\); in cases where the other has no muon identification \((\mathcal{R}_\mu = 0)\), in order to suppress fake muon tracks, the cosine of the polar angle of each muon track in the \(K^+ K^- \mu^+ \mu^-\) CM frame is required to be less than 0.7. Events with \(\gamma\) conversions are removed by requiring \(\mathcal{R}_e < 0.75\) for the \(K^+ K^-\) tracks.

In \(J/\psi \rightarrow e^+ e^-\), \(\gamma\) conversion events are further suppressed by requiring the invariant mass of \(K^+ K^-\) to be larger than 1.05 GeV/c\(^2\); this also removes the events with a \(\phi\) meson in the final state. In \(J/\psi \rightarrow \mu^+ \mu^-\), the invariant mass of \(K^+ K^-\) is required to be outside a \(\pm 10\) MeV/c\(^2\) interval around the \(\phi\) nominal mass to remove events with a \(\phi\) meson in the final state, possibly produced via \(e^+ e^- \rightarrow \gamma \gamma^* \gamma^* \rightarrow \gamma \phi \ell^+ \ell^-\). There is only one combination of \(K^+ K^- \ell^+ \ell^-\) in each event after the above event selections.

The ISR events are identified by the requirement \([M_{\text{rec}}^2] < 1.0\) (GeV/c\(^2\))^\(2\), where \(M_{\text{rec}}^2 = (P_{CM} - P_K - P_K(fl - P_{\ell^+} - P_{\ell^-})^2\) and \(P_i\) represents the four-momentum of the corresponding particle in the \(e^+ e^-\) CM frame. Clear \(J/\psi\) signals are observed in both \(J/\psi \rightarrow e^+ e^-\) and \(J/\psi \rightarrow \mu^+ \mu^-\) modes, as shown in Fig. 1. We define the \(J/\psi\) signal region as \(3.06 < M(\ell^+ \ell^-) < 3.14\) GeV/c\(^2\) (with the mass resolution of lepton pairs being about 17 MeV/c\(^2\)), and the \(J/\psi\) mass sideband as \(2.91 < M(\ell^+ \ell^-) < 3.03\) or \(3.17 < M(\ell^+ \ell^-) < 3.29\) GeV/c\(^2\), which is three times the width of the signal region. Here, final state radiation and bremsstrahlung energy loss are recovered by adding the four-momentum of photons detected within a \(5^\circ\) cone around the electron and positron direction in the \(e^+ e^-\) invariant mass calculation.

![FIG. 1: Invariant mass distributions of (a) \(e^+ e^-\) and (b) \(\mu^+ \mu^-\) for selected \(K^+ K^- \ell^+ \ell^-\) candidates. The curves show the best fits to the mass spectra, and the arrows show the required \(J/\psi\) signal regions defined in the text.](image)

For selection of \(e^+ e^- \rightarrow K_S^0 K_S^0 \ell^+ \ell^-\) events within the same data sample, all the selection criteria are the same as for \(K^+ K^-\) except that the selection of \(K^+ K^-\) is replaced by the selection of two \(K_S^0\). For a \(K_S^0\) candidate decaying into \(\pi^+ \pi^-\), we require that the invariant mass of the \(\pi^+ \pi^-\) pair lie within a \(\pm 11\) MeV/c\(^2\) interval around the \(K_S^0\) nominal mass, which contains around 95% of the signal according to the MC simulation, and that the pion pair has a displaced vertex and flight direction consistent with a \(K_S^0\) originating from the interaction point [22].
Figure 2 shows the $K^+K^-\ell^+\ell^-$ and $K_S^0K_S^0\ell^+\ell^-$ invariant mass distributions after applying the above selection, together with the backgrounds estimated from the normalized $J/\psi$ mass sidebands. The $K^+K^-\ell^+\ell^-$ invariant mass distribution is similar to that in Ref. [13] and shows a broad enhancement around 4.4-5.5 GeV/c$^2$. In addition, there are 3 events near $\sqrt{s} = 4.26$ GeV. It is evident from the figure that the background estimated from the $J/\psi$ mass sidebands is low, which indicates that the background from the non-$J/\psi$ final states is small. The other backgrounds not shown in the sidebands include: (1) $K^+K^-J/\psi$ with $J/\psi$ decaying into final states other than lepton pairs; (2) $XJ/\psi$, with $X$ not being $K^+K^-$. The number of these background events is found to be small from MC simulation and thus they are neglected. Non-ISR production of the $e^+e^- \rightarrow K^+K^-J/\psi$ process, such as $e^+e^- \rightarrow \gamma\gamma^{*}\gamma \rightarrow \gamma\phi J/\psi$, is calculated to be small [24] and is neglected. For the $M(K_S^0K_S^0J/\psi)$ distribution, there are only 10 signal candidate events between 4.6 and 5.5 GeV/c$^2$ with 4 background events estimated from the $J/\psi$ mass sidebands. In other regions, the number of events in the $J/\psi$ signal region is about the same as expected from the normalized sideband events.

III. CROSS SECTIONS

The $e^+e^- \rightarrow K^+K^-J/\psi$ cross section at each energy point is calculated using

$$\sigma_i = \frac{n_{i}^{\text{obs}} - f \times n_{i}^{\text{bkg}}}{\mathcal{L}_i \cdot \epsilon_i \cdot \mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)}.$$  

where $n_{i}^{\text{obs}}, n_{i}^{\text{bkg}}, f, \epsilon_i$, and $\mathcal{L}_i$ are the number of observed events in data, the number of background events estimated from the $J/\psi$ sidebands, the scale factor ($f = 1/3$), the detection efficiency, and the effective ISR luminosity obtained from the QED calculation [25] in the $i$-th energy bin, respectively; $\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-) = 11.87\%$ is taken from Ref. [14]. According to the MC simulation, the
FIG. 3: (a) The distribution of the squared mass recoiling against the $K^+K^-J/\psi$ system distribution and (b) the polar angle distribution of the $K^+K^-J/\psi$ system in the $e^+e^-$ CM frame for the selected $K^+K^-J/\psi$ events with invariant masses between 4.0 and 6.0 GeV/$c^2$. The points with error bars are data with the normalized $J/\psi$ mass sidebands subtracted; the solid histograms are MC simulated events.

efficiency for $K^+K^-J/\psi$ ($K_S^0K_S^0J/\psi$) increases smoothly from 1.69% (0.30%) at 4.2 GeV/$c^2$, 7.53% (0.56%) at 4.6 GeV/$c^2$, 11.50% (1.04%) at 5.2 GeV/$c^2$, to 14.93% (1.45%) at 5.8 GeV/$c^2$. Figure 4 shows the measured cross sections for $e^+e^- \rightarrow K^+K^-J/\psi$, where the error bars indicate the combined statistical errors of the signal and the background events, following the procedure in Ref. [26]. The measured $e^+e^- \rightarrow K^+K^-J/\psi$ cross sections are consistent with previously published results [13] with improved precision. Similarly, the $e^+e^- \rightarrow K_S^0K_S^0J/\psi$ cross section is calculated. Since the number of $K_S^0K_S^0J/\psi$ signal events is very small, we give an average cross section for $e^+e^- \rightarrow K_S^0K_S^0J/\psi$ of $1.8 \pm 0.6\,(\text{stat.})$ pb between 4.4 and 5.2 GeV/$c^2$. The result is consistent with the previously published result of $1.8_{-1.1}^{+1.4}\,(\text{stat.})$ pb [13] with better precision. Tables I and II list the final results and all the information used in the cross section calculation for $e^+e^- \rightarrow K^+K^-J/\psi$ and $K_S^0K_S^0J/\psi$, respectively.

FIG. 4: The measured $e^+e^- \rightarrow K^+K^-J/\psi$ cross sections for CM energies up to 6.0 GeV (points with error bars). The errors are statistical and are determined by the numbers of signal and background events; a 7.8% systematic error that is common for all data points is not included.

Systematic error sources and their contributions in the cross section measurements are summarized in Table III. The lepton pair identification uncertainties, measured from a pure control
TABLE I: Cross sections (σ) of $e^+e^- \rightarrow K^+K^- J/\psi$. We also list the $e^+e^-$ center-of-mass energy ($\sqrt{s}$), number of observed events ($n^{\text{obs}}$), number of backgrounds estimated from $J/\psi$ mass sidebands ($n^{\text{bkg}}$), detection efficiency ($\epsilon$), and effective ISR luminosity ($\mathcal{L}$). All values are calculated for 50 MeV bin size and $\sqrt{s}$ is the central value of the bin. The first errors are statistical and the second ones systematic. For the bins with lower limit at zero at 68.3% confidence interval, a confidence interval is given with systematic error included [26].

| $\sqrt{s}$ (GeV) | $n^{\text{obs}}$ | $n^{\text{bkg}}$ | $\mathcal{L}$ (pb$^{-1}$) | $\sigma$ (pb) | $\sqrt{s}$ (GeV) | $n^{\text{obs}}$ | $n^{\text{bkg}}$ | $\mathcal{L}$ (pb$^{-1}$) | $\sigma$ (pb) |
|------------------|-----------------|-----------------|-----------------|-------------|------------------|-----------------|-----------------|-----------------|-------------|
| 4.175            | 14              | 0               | 207             | 3.6$^{+3.2}_{-2.6}$ ± 0.3 | 5.125           | 9               | 2               | 286             | 2.2$^{+1.0}_{-0.8}$ ± 0.2 |
| 4.225            | 1               | 2.25            | 210             | 1.8$^{+1.3}_{-1.2}$ ± 0.2 | 5.175           | 6               | 3               | 291             | 1.3$^{+0.7}_{-0.6}$ ± 0.1 |
| 4.275            | 2               | 3.24            | 214             | [0, 2.3]       | 5.225           | 5               | 3               | 296             | 1.0$^{+0.7}_{-0.6}$ ± 0.1 |
| 4.325            | 0               | 4.13            | 218             | [0, 1.3]       | 5.275           | 9               | 7               | 301             | 1.6$^{+0.9}_{-0.8}$ ± 0.2 |
| 4.375            | 0               | 4.91            | 221             | [0, 1.1]       | 5.325           | 6               | 7               | 306             | 0.8$^{+0.8}_{-0.7}$ ± 0.1 |
| 4.425            | 4               | 5.61            | 225             | 2.7$^{+1.2}_{-1.1}$ ± 0.3 | 5.375           | 17              | 2               | 126             | 3.5$^{+1.0}_{-1.0}$ ± 0.3 |
| 4.475            | 12              | 6.23            | 229             | 7.1$^{+2.6}_{-2.0}$ ± 0.6 | 5.425           | 7               | 7               | 317             | 1.0$^{+0.7}_{-0.6}$ ± 0.1 |
| 4.525            | 8               | 6.78            | 233             | 3.9$^{+1.8}_{-1.6}$ ± 0.4 | 5.475           | 3               | 3               | 323             | 0.4$^{+0.5}_{-0.4}$ ± 0.1 |
| 4.575            | 3               | 7.27            | 237             | 1.1$^{+1.1}_{-1.0}$ ± 0.1 | 5.525           | 7               | 4               | 352             | 1.1$^{+0.7}_{-0.6}$ ± 0.1 |
| 4.625            | 9               | 7.72            | 241             | 3.8$^{+1.8}_{-1.3}$ ± 0.3 | 5.575           | 5               | 4               | 334             | 0.7$^{+0.6}_{-0.5}$ ± 0.1 |
| 4.675            | 7               | 8.13            | 245             | 2.8$^{+1.2}_{-1.1}$ ± 0.3 | 5.625           | 3               | 6               | 340             | [0, 0.7]       |
| 4.725            | 3               | 8.50            | 249             | 0.8$^{+0.6}_{-0.5}$ ± 0.1 | 5.675           | 4               | 1               | 346             | 0.6$^{+0.5}_{-0.4}$ ± 0.1 |
| 4.775            | 16              | 8.85            | 253             | 5.9$^{+1.7}_{-1.5}$ ± 0.5 | 5.725           | 2               | 3               | 353             | 0.2$^{+0.4}_{-0.2}$ ± 0.1 |
| 4.825            | 2               | 9.18            | 258             | 0.7$^{+0.5}_{-0.4}$ ± 0.1 | 5.775           | 3               | 4               | 359             | 0.3$^{+0.3}_{-0.3}$ ± 0.1 |
| 4.875            | 5               | 9.49            | 262             | 1.5$^{+1.0}_{-0.8}$ ± 0.2 | 5.825           | 4               | 15              | 366             | 0.4$^{+0.4}_{-0.3}$ ± 0.1 |
| 4.925            | 9               | 9.80            | 267             | 2.5$^{+1.2}_{-1.1}$ ± 0.2 | 5.875           | 5               | 6               | 315             | 0.5$^{+0.3}_{-0.3}$ ± 0.1 |
| 4.975            | 12              | 10.1            | 271             | 3.4$^{+1.3}_{-1.2}$ ± 0.3 | 5.925           | 4               | 5               | 380             | 0.3$^{+0.2}_{-0.1}$ ± 0.1 |
| 5.025            | 7               | 10.4            | 276             | 1.7$^{+1.0}_{-0.9}$ ± 0.2 | 5.975           | 3               | 4               | 387             | 0.2$^{+0.4}_{-0.3}$ ± 0.1 |
| 5.075            | 11              | 10.7            | 281             | 2.9$^{+1.0}_{-1.0}$ ± 0.3 |                  |                  |                  |                  |                |

sample of $e^+e^- \rightarrow \gamma_{\text{ISR}}\psi(2S)$ events with $\psi(2S) \rightarrow \pi^+\pi^- J/\psi$, $J/\psi \rightarrow \ell^+\ell^-$, are 3.5% and 1.8% for $e^+e^-$ and $\mu^+\mu^-$, respectively [1]. The uncertainty due to kaon particle identification is 1.2% for each kaon. Tracking efficiency uncertainties are estimated to be 1.3% per kaon track and 0.35% per lepton track, which are fully correlated in the momentum and angle regions of interest for signal events. The systematic uncertainty in the $K_S^0$ mass window and $|M^2_{\text{rec}}|$ requirements are also estimated using pure $\psi(2S) \rightarrow \pi^+\pi^- J/\psi$ events. It is found that MC efficiencies are higher than in data by $(2.1 \pm 0.7)\%$. We take 2.8% as the systematic uncertainty for each $K_S^0$ selection. The uncertainties associated with the $J/\psi$ mass window and $|M^2_{\text{rec}}|$ requirements are also estimated using pure $\psi(2S) \rightarrow \pi^+\pi^- J/\psi$ events. It is found that MC efficiencies are higher than in data by $(4.5 \pm 0.4)\%$ in the $e^+e^-$ mode and $(4.1 \pm 0.2)\%$ in the $\mu^+\mu^-$ mode. The differences in efficiencies are corrected and the uncertainties in the correction factors are taken as systematic errors. They contribute 0.6% for the $e^+e^-$ and 0.3% for the $\mu^+\mu^-$ mode in total for the $J/\psi$ mass window together with the $|M^2_{\text{rec}}|$ requirements [1]. Estimating the backgrounds using different $J/\psi$ mass sidebands results in a change of background events at the 0.12/50 MeV/$c^2$ level for $K^+K^-J/\psi$ and 0.008/50 MeV/$c^2$ level for $K^0_SK_S\bar{J}/\psi$, corresponding to an average change of about 2.6% for $K^+K^-J/\psi$ and 14%
TABLE II: Cross sections ($\sigma$) of $e^+e^- \rightarrow K^0_S K^0_S J/\psi$. We also list the $e^+e^-$ center-of-mass energy ($\sqrt{s}$), number of observed events ($n^{\text{obs}}$), number of backgrounds estimated from $J/\psi$ mass sidebands ($n^{\text{bkg}}$), detection efficiency ($\epsilon$), and effective ISR luminosity ($L$). All values are calculated for 50 MeV bin size and $\sqrt{s}$ is the central value of the bin. As the number of $K^0_S K^0_S J/\psi$ signal events is small, a 68.3% confidence interval for the measured cross section is given with systematic error included [26].

| $\sqrt{s}$ (GeV) | $n^{\text{obs}}$ | $n^{\text{bkg}}$ | $\epsilon$ ($\%$) | $L$ (pb$^{-1}$) | $\sigma$ (pb) | $\sqrt{s}$ (GeV) | $n^{\text{obs}}$ | $n^{\text{bkg}}$ | $\epsilon$ ($\%$) | $L$ (pb$^{-1}$) | $\sigma$ (pb) |
|------------------|------------------|------------------|------------------|-----------------|-------------|------------------|------------------|------------------|------------------|-----------------|-------------|
| 4.175            | 0                | 0                | 0.26             | 207             | [0, 21]      | 5.125           | 0                | 0                | 0.96             | 286             | [0, 4.0] |
| 4.225            | 0                | 0                | 0.30             | 210             | [0, 18]      | 5.175           | 1                | 1                | 1.00             | 291             | [0, 6.7] |
| 4.275            | 0                | 0                | 0.34             | 214             | [0, 16]      | 5.225           | 0                | 0                | 1.03             | 296             | [0, 3.6] |
| 4.325            | 0                | 0                | 0.37             | 218             | [0, 10]      | 5.275           | 1                | 0                | 1.07             | 301             | [0.7, 7.1] |
| 4.375            | 0                | 0                | 0.41             | 221             | [0, 13]      | 5.325           | 2                | 2                | 1.11             | 306             | [0.7, 8.7] |
| 4.425            | 0                | 0                | 0.44             | 225             | [2.5, 23]    | 5.375           | 0                | 1                | 1.15             | 311             | [0, 2.2] |
| 4.475            | 0                | 0                | 0.48             | 229             | [0, 10]      | 5.425           | 0                | 0                | 1.18             | 317             | [0, 3.0] |
| 4.525            | 0                | 0                | 0.52             | 233             | [0, 9.2]     | 5.475           | 0                | 1                | 1.22             | 323             | [0, 2.0] |
| 4.575            | 0                | 0                | 0.55             | 237             | [0, 8.4]     | 5.525           | 1                | 1                | 1.26             | 328             | [0, 4.7] |
| 4.625            | 0                | 0                | 0.59             | 241             | [0, 7.8]     | 5.575           | 1                | 3                | 1.30             | 334             | [0, 3.4] |
| 4.675            | 0                | 1                | 0.63             | 245             | [0, 5.0]     | 5.625           | 0                | 5                | 1.34             | 340             | [0, 1.0] |
| 4.725            | 2                | 1                | 0.66             | 249             | [2.5, 20]    | 5.675           | 0                | 2                | 1.37             | 346             | [0, 1.3] |
| 4.775            | 0                | 0                | 0.70             | 253             | [0, 6.2]     | 5.725           | 1                | 1                | 1.41             | 353             | [0, 3.9] |
| 4.825            | 1                | 2                | 0.74             | 258             | [0, 8.5]     | 5.775           | 0                | 2                | 1.45             | 359             | [0, 1.2] |
| 4.875            | 1                | 2                | 0.77             | 262             | [0, 7.9]     | 5.825           | 0                | 2                | 1.49             | 366             | [0, 1.1] |
| 4.925            | 1                | 0                | 0.81             | 267             | [1.1, 11]    | 5.875           | 0                | 2                | 1.53             | 373             | [0, 1.1] |
| 4.975            | 0                | 1                | 0.85             | 271             | [0, 3.3]     | 5.925           | 1                | 4                | 1.56             | 380             | [0, 2.5] |
| 5.025            | 1                | 0                | 0.89             | 276             | [1.0, 9.4]   | 5.975           | 0                | 3                | 1.60             | 387             | [0, 0.7] |
| 5.075            | 0                | 0                | 0.92             | 281             | [0, 4.3]     |                  |                  |                  |                  |                 | |

for $K^0_S K^0_S J/\psi$ in the cross section. Belle measures the total luminosity with a precision of 1.4% using Bhabha events. The PHOKHARA generator calculates the ISR photon radiator function with 0.1% accuracy [17]. The dominant uncertainties due to the generator come from the three-body decay dynamics; there is no good model to describe the $K^+K^-$ mass spectrum. Simulations with modified $K^+K^-$ invariant mass distributions such as $M(\pi^+\pi^-)$ in $\psi(2S) \rightarrow \pi^+\pi^- J/\psi$ [18] yield efficiencies that are higher by 3.3-4.8% for different $K^+K^- J/\psi$ masses. We take 4.8% as a conservative estimation for the $K^+K^- J/\psi$ mass values. Similarly, we take 4.5% for the $K^0_S K^0_S J/\psi$ mode. The angular distributions of the final state particles for selected $K^+K^- J/\psi$ events from data are consistent with the MC simulations and no evidence is found for non-S-wave components. The selected data sample contains at least four charged tracks and so the trigger efficiency is higher than 98% according to MC simulation. A 1.0% systematic error is assigned for the trigger uncertainty. The uncertainty of $B(J/\psi \rightarrow \ell^+\ell^-) = B(J/\psi \rightarrow e^+e^-) + B(J/\psi \rightarrow \mu^+\mu^-)$ is taken as 1.0% from Ref. [14]. The uncertainty of $B(K_S^0 \rightarrow \pi^+\pi^-)$ is neglected. Finally, the MC statistical error on the efficiency is 1.5%. Assuming that all the sources are independent and adding them in quadrature, we obtain a total systematic error on the cross section of 7.8% for the $K^+K^- J/\psi$ and 16% for $K^0_S K^0_S J/\psi$ final states.
TABLE III: Systematic errors in $e^+e^- \rightarrow K^+K^-J/\psi$ and $K_S^0K_S^0J/\psi$ cross section measurements.

| Source                        | $K^+K^-J/\psi$ (%) | $K_S^0K_S^0J/\psi$ (%) |
|-------------------------------|--------------------|-------------------------|
| Particle identification       | 3.6                | 2.6                     |
| Tracking                      | 3.3                | 0.7                     |
| $K_S^0$ selection             | —                  | 5.6                     |
| $J/\psi$ mass and $M_{\text{rec}}^2$ selection | 0.4 | 0.4 |
| Background estimation         | 2.6                | 14                      |
| Integrated luminosity         | 1.4                | 1.4                     |
| Generator                     | 4.8                | 4.5                     |
| Trigger efficiency            | 1.0                | 1.0                     |
| Branching fractions           | 1.0                | 1.0                     |
| MC statistics                 | 1.5                | 1.5                     |
| Sum in quadrature             | 7.8                | 16                      |

IV. RESONANT STRUCTURES

The unbinned maximum likelihood fit performed in Ref. [13] is applied to the $K^+K^-J/\psi$ mass spectrum in Fig. 2(a). The theoretical shape is multiplied by the efficiency and effective luminosity, which are functions of the $K^+K^-J/\psi$ invariant mass. The BW function for a spin-1 resonance decaying into a final state $f$ with mass $M$, total width $\Gamma_{\text{tot}}$ and partial width $\Gamma_{e^+e^-}$ to $e^+e^-$ is

$$\sigma(s) = \frac{M^2}{s} \frac{12\pi \Gamma_{e^+e^-} B(R \rightarrow f) \Gamma_{\text{tot}}}{(s-M^2)^2 + M^2 \Gamma_{\text{tot}}^2} \rho(\sqrt{s}),$$

where $B(R \rightarrow f)$ is the branching fraction of the resonance to the final state $f$, and $\rho(\sqrt{s})$ is the three-body decay phase space factor for $X \rightarrow K^+K^-J/\psi$. We attempt to fit the $K^+K^-J/\psi$ invariant mass spectrum using two different parameterizations of the signal shape: (1) a single BW function plus a background term; (2) a coherent sum of a BW function and a $\psi(4415)$ component with mass and width fixed at their world average values [14] plus a background term. The fit results are shown in Fig. 5. The results of the fit for the BW parameters $[M = (4482 \pm 45) \text{ MeV}/c^2$, $\Gamma_{\text{tot}} = (432 \pm 56) \text{ MeV}$ for model (a) and $M = (4747 \pm 117) \text{ MeV}/c^2$, $\Gamma_{\text{tot}} = (671 \pm 86) \text{ MeV}/c^2$ for model (b)] are consistent with the previously published results within about 2$\sigma$, but the goodness of the fit ($\chi^2/ndf = 39/13 = 3.0$ for model (a) and $\chi^2/ndf = 30/11 = 2.7$ for model (b)) is marginal. (Here, $ndf$ is the number of degrees of freedom). Thus, our two models can not describe the data well with the increased statistics. Here, in determining the goodness of each fit, we bin the data so that the expected number of events in a bin is at least seven. Adding a coherent $Y(4260)$ amplitude in the fit with mass and width fixed at the latest Belle measurement [1] yields an upper limit on $B(Y(4260) \rightarrow K^+K^-J/\psi) \Gamma(Y(4260) \rightarrow e^+e^-) < 1.7 \text{ eV}/c^2$ at 90% confidence level. A similar fit to the $K_S^0K_S^0J/\psi$ invariant mass spectrum with a $Y(4260)$ amplitude yields an upper limit on $B(Y(4260) \rightarrow K_S^0K_S^0J/\psi) \Gamma(Y(4260) \rightarrow e^+e^-) < 0.85 \text{ eV}/c^2$ at 90% confidence level.

Possible intermediate states are studied by examining the Dalitz plot of the selected $K^+K^-J/\psi$ candidate events. Figure 6 shows the Dalitz plots of events in the $J/\psi$ signal region and $J/\psi$ mass sidebands. Figure 7 shows a projection of the $M(K^+K^-)$, $M(K^+J/\psi)$, and $M(K^-J/\psi)$ invariant mass distributions. Background events estimated from the normalized $J/\psi$ mass sidebands are shown as the shaded histograms. No obvious structures are observed in the $K^\pm J/\psi$ system. The
FIG. 5: Fits to the $K^+K^-J/\psi$ invariant mass distribution. The open histograms are the selected data in the $J/\psi$ signal region while the shaded histograms show the normalized $J/\psi$ sideband events. The solid curves show the best fit to the data and sideband background with one BW function (a) and the coherent sum of a BW function and the $\psi(4415)$ component (b).

low statistics prevent us from extracting additional information on the three-body dynamics.

FIG. 6: Dalitz plots for the selected $K^+K^-J/\psi$ events for $4.4 < M(K^+K^-J/\psi) < 5.5$ GeV/$c^2$. The left panel is for events in the $J/\psi$ signal region while the right is from the $J/\psi$ mass sidebands (not normalized).

V. SUMMARY

The cross sections of $e^+e^- \to K^+K^-J/\psi$ and $K_S^0K_S^0J/\psi$ are measured from threshold to 6.0 GeV using the full Belle data sample. There are clear $K^+K^-J/\psi$ signal events; however fits that were tried before [13] with a smaller data set using either a single BW function or using the $\psi(4415)$ plus a second BW function are inadequate for the full data sample. Possible intermediate states for the selected $K^+K^-J/\psi$ events are also investigated by examining the Dalitz plot but no clear structure is observed in the $K^\pm J/\psi$ system. Since there are only a few $K_S^0K_S^0J/\psi$ signal events and no structure is observed in the $K_S^0K_S^0J/\psi$ mass spectrum, the Dalitz plot of $K_S^0K_S^0J/\psi$ events is not examined. A larger data sample is necessary to obtain more information about possible structures in the $K^+K^-J/\psi$, $K_S^0K_S^0J/\psi$, $K^+K^-$ and $K^\pm J/\psi$ systems.
FIG. 7: Invariant mass distributions of (a) $K^+K^-$, (b) $K^+J/\psi$, and (c) $K^-J/\psi$ for $K^+K^-J/\psi$ events with $4.4 < M(K^+K^-J/\psi) < 5.5$ GeV/$c^2$. Solid histograms are for events in the $J/\psi$ signal region, and the shaded histograms are normalized background from the $J/\psi$ mass sidebands.

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