Cutting the Unnecessary Long Tail: Cost-Effective Big Data Clustering in the Cloud

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Abstract—Clustering big data often requires tremendous computational resources where cloud computing is undoubtedly one of the promising solutions. However, the computation cost in the cloud can be unexpectedly high if it cannot be managed properly. The long tail phenomenon has been observed widely in the big data clustering area, which indicates that the majority of time is often consumed in the middle to late stages in the clustering process. In this research, we try to cut the unnecessary long tail in the clustering process to achieve a sufficiently satisfactory accuracy at the lowest possible computation cost. A novel approach is proposed to achieve cost-effective big data clustering in the cloud. By training the regression model with the sampling data, we can make widely used k-means and EM (Expectation-Maximization) algorithms stop automatically at an early point when the desired accuracy is obtained. Experiments are conducted on four popular data sets and the results demonstrate that both k-means and EM algorithms can achieve high cost-effectiveness in the cloud with our proposed approach. For example, in the case studies with the much more efficient k-means algorithm, we find that achieving a 99% accuracy needs only 47.71%-71.14% of the computation cost required for achieving a 100% accuracy while the less efficient EM algorithm needs 16.69%-32.04% of the computation cost. To put that into perspective, in the United States land use classification example, our approach can save up to $94,687.49 for the government in each use.

Index Terms—Cloud computing, cost-effectiveness, clustering algorithms, big data, data mining.

1 INTRODUCTION

The long tail refers to the phenomenon where the portion of the distribution has a large number of occurrences far from the head or central part of the distribution, which is commonly observed in recommendation systems and data mining [1], [2]. In recent years, with the explosive growth of data in many areas such as remote sensing [3], [4], business [5], and bioinformatics [6], the capability for data generation becomes so powerful and enormous. Clustering algorithms have been widely used as one of the most powerful meta-learning tools for accurate analysis of massive volumes of data generated by modern devices. The main goal of clustering is to categorize data points into clusters such that those grouped in the same cluster are similar according to specific metrics. During the clustering process, it is usual that the clusters are formed quickly at the early stage while changes slowly during the middle to late stages. This is the long tail in clustering [7].

In the area of clustering, there have been lots of attempts to analyze and categorize the data for the huge number of applications. However, one of the major issues in using clustering algorithms is that it often requires tremendous computational resources especially when processing large-scale data sets. To illustrate this, we use the k-means algorithm to cluster remote sensing images. For $k$ clusters and $p$ pixels, a total of $k \times p$ distances need be computed at each iteration. For example, for 10 classes and 40000 (200 $\times$ 200) pixels, 50 iterations of the k-means clustering require 20 million multiplications for every image. Usually, the remote sensing data sets are huge and consist of tens of thousands of images such as SAT-6 [8], AID [9], NWPU-RESISC45 [10]. As a result, processing such data is undoubtedly computationally intensive and extremely costly.

Small and medium-sized organizations usually cannot afford the exorbitant in-house IT infrastructure for processing such a large amount of data. Naturally, cloud computing, the latest distributed computing paradigm which eliminates the need to maintain expensive computing hardware, dedicated space, and software, becomes the best choice for them [11].

Cloud computing adopts the pay-as-you-go model, where users are charged flexibly according to the usage of cloud services such as computational resources. However, the computation cost in the cloud can be unexpectedly high if users cannot manage it properly, which also becomes a bottleneck for big data mining in the cloud. For instance, running 50 m4-2xlarge EC2 virtual machine (VM) instances in Amazons Sydney datacenter costs $18,000 per month [12].

In most clustering situations, it is not always necessary to achieve the optimal solution because users often do not need 100%. Take the marketing for example, based on various customer interests, age and product holding information, clustering techniques have been used for creating customer groups. In this situation, a reasonable margin of inaccuracy is acceptable because marketers do not need their customers to be grouped with 100% accuracy. As long as they have
a general picture of the clustering result, they are able to
make a decision. In fact, there will never be completely ac-
rate, e.g., weather forecasting or land use statistics. In such
scenarios, stopping the clustering process at a reasonable
point is important in saving computation costs if it is more
preferable to achieve a sufficiently satisfied accuracy at a
low computation cost than a 100% accuracy at a high cost.

Thus, cutting the unnecessary long tail in the clustering
process is a promising solution to cost-effective clustering.
In other words, we need to study how to achieve a suffi-
ciently satisfactory clustering accuracy at the lowest possible
computation cost.

Cost-effective clustering in the cloud allows big data
analytics to be applied in a broader range of fields by more
businesses and organizations, especially small and medium-
sized ones with the limited budget. He et al. observed the
long tail phenomenon and studied the cost effectiveness
of the k-means algorithm in the cloud. They found that
achieving 99% accuracy with the k-means algorithm only
needs a bit more than 20% of computation time on av-
average [7]. However, when to stop the k-means algorithm
automatically with the desired accuracy has not been well
investigated by researchers up to now.

There is a variety of clustering techniques that can be
adopted for exploration and demonstration of the cost ef-
ficacy of big data clustering in the cloud. Among the
top 10 data mining algorithms discussed by Wu et al. [13], k-
means [14] and EM (Expectation Maximization) algorithms
[15] belong to the field of clustering. Furthermore, k-means
and EM are both iterative algorithms and converge to the
final (optimal) result iteratively [16], [17], which provides
possibilities for us to calculate the accuracy of the inter-
mediate clustering result at each iteration of the clustering
process. Therefore, we choose k-means and EM algorithms
to explore and demonstrate the cost-effective clustering in
the cloud.

The contributions of the paper are as follows:

1) We demonstrated the long tail phenomenon in the
clustering process, and defined the cost effective-
ness problem of k-means and EM clustering algo-
rithms in the cloud.
2) To the best of our knowledge, this is the first pa-
er to achieve cost-effective clustering in the cloud
through cutting the unnecessary long tail. We pro-
aposed a regression model between the change rate
of objective function and clustering accuracy.
3) We compared the excellent performance of cost ef-
ficacy of k-means and EM algorithms on mul-
tiple benchmark data sets, and discussed the threats
to validity of the results.

The remainder of the paper is organized as follows. Section
2 presents a motivating example and analyzes the research
problem. Then, Section 3 describes the methodologies used
in the cost-effectiveness problem and Section 4 proposes
a novel approach for cost-effective big data clustering in
the cloud. Section 5 displays the results of experiments
conducted on different data sets. Section 6 surveys the
related work. Finally, Section 7 addresses the conclusions
and future work.
Due to the long tail phenomenon (see Section 3.4) in the clustering process, a sufficient clustering accuracy may be obtained within a short time. After that, incremental accuracy improvement usually takes a relatively long time in the remainder of the clustering process. Thus, we need to consider the utilization of this phenomenon and find an appropriate point to terminate the clustering process to achieve satisfactory accuracy at a low cost.

3 Methodology

This section presents our study of cost-effective clustering, including the candidate clustering techniques, the accuracy calculation method, the cloud cost computing model, and cost-effective clustering analysis. Clustering is a powerful method for analyzing massive volumes of data. The main idea of clustering is to minimize a certain criterion function usually taken up as a function of the deviations among all patterns from their respective cluster centers. Usually, the minimization of the criterion function is sought to utilize an iterative scheme that starts with a chosen initial cluster configuration of the data, then alters the cluster membership in an iterative manner to obtain a better configuration. Appendix A lists the key notations used in this paper.

3.1 Candidate Clustering Techniques

Clustering is an unsupervised method for finding patterns based on features [20]. Usually, a feature point can be represented by a vector \( x = (x_1, x_2, ..., x_d) \). Based on the distance measure among feature vectors, a label will be assigned to each feature. Here, we take the popular k-means and EM algorithms as examples to demonstrate the cost effectiveness of big data clustering in the cloud.

3.1.1 K-means Algorithm

The k-means algorithm proposed by Mac Queen [14] is one of the simplest and most popular techniques in data mining. It begins with \( k \) initial centers and each point will be assigned with a label based on the distance between the point and the cluster centers. The steps of the k-means algorithm are as follows:

Step 1: Select \( k \) points as initial centers \( C = \{c_1, c_2, ..., c_k\} \).

Step 2: For each \( i \in \{1, 2, ..., k\} \), set cluster \( C_i \) as the set of data points that are closer to \( c_i \) than to \( c_j \) for all \( j \neq i \).

Step 3: Recompute \( c_i \) as the center of \( C_i \):

\[
    c_i = \frac{1}{|C_i|} \sum_{x \in C_i} x. \tag{1}
\]

Step 4: Repeat Steps 2 and 3 until \( C \) no longer changes. During the process, let \( \mu_i \) represent the mean of cluster \( C_i \). Then the goal of k-means is to minimize the criterion function in an iterative manner:

\[
    J = \sum_{i=1}^{k} \sum_{x \in C_i} \|x - \mu_i\|^2 \tag{2}
\]

In Equation (2), the squared Euclidean distance is adopted to represent the metric of \( \|x_i - \mu_k\|^2 \) due to its computational simplicity since the cluster at each iteration can be calculated in a straightforward manner. The time complexity of the k-means algorithm is \( O(nkd_i) \), where \( n \) is the number of \( d \) dimensional data points in the data set, \( k \) is the number of clusters and \( i \) is the number of iterations for the clustering process to complete (i.e. converge).

3.1.2 EM Algorithm

The Expectation-Maximization (EM) algorithm is designed to estimate the maximum likelihood parameters of a statistical model in many situations, such as the one where the equations cannot be solved. EM approximates the unknown model parameters iteratively with the Expectation step (E step) and the Maximization step (M step) which are as follows:

**E step** calculates the expected value of the log-likelihood function, with respect to the conditional distribution of \( Z \) given \( X \) under the current estimate of the parameters \( \theta^t \):

\[
    Q(\theta | \theta^t) = E_{Z|X,\theta^t}(\log L(\theta; X, Z)) \tag{3}
\]

**M step** finds the parameters that maximize this quantity:

\[
    \theta_{t+1} = \arg\max_{\theta} Q(\theta | \theta^t) \tag{4}
\]

The EM algorithm seeks to find the maximum likelihood estimation (MLE) by iterating the above two steps.

3.2 Accuracy Calculation

Accuracy is a crucial measurement for evaluating the effectiveness of big data clustering. For the purpose of demonstrating the gradual increase of the clustering accuracy iteration by iteration, we use the final clustering result as the reference partition noted by \( P_f \) as 100% accuracy. Through the comparison between the clustering results achieved at each iteration of the algorithm, we can demonstrate how the accuracy of the intermediate partition result \( P_i \in \{P_1, P_2, ..., P_f\} \) increases.

The accuracy can be measured by the similarity between \( P_i \) and \( P_f \). In our research, we use the Rand Index [21] to assess the similarity, which is a popular accuracy calculation method in the data clustering field. The Rand Index measures the similarity between two data clustering partitions. Each partition is viewed as a collection of \( n \times (n - 1)/2 \) pairs of elements, where \( n \) is the size of the data set. For each pair of data points, a partition either assigns them to the same cluster or different clusters. Thus, the similarity between partitions \( P_1 \) and \( P_2 \) can be calculated as follows:

\[
    \text{Rand}(P_1, P_2) = \frac{n_{11} + n_{00}}{n_{00} + n_{01} + n_{10} + n_{11}} = \frac{n_{11} + n_{00}}{\binom{n}{2}} \tag{5}
\]

where:

- \( n_{11} \): the number of pairs of elements that are placed in the same clusters both in \( P_1 \) and \( P_2 \);
- \( n_{00} \): the number of pairs of elements that are placed in the different clusters both in \( P_1 \) and \( P_2 \);
- \( n_{01} \): the number of pairs of elements that are placed in the same clusters in \( P_1 \) but in different clusters in \( P_2 \);
- \( n_{10} \): the number of pairs of elements that are placed in different clusters in \( P_1 \), but in the same clusters in \( P_2 \).

Using the Rand Index as the similarity calculation measure, we can compute the clustering accuracy at each iteration of the clustering process. Take Fig. 1 for example, for the
The EM algorithm is a specific algorithm used in the final iteration of clustering processes, where the value of Rand Index increases with iterations and at the final iteration of clustering process, where the computation cost is calculated by the cost models offered by cloud vendors. In this research, we use Amazon’s Elastic Compute Cloud (Amazon EC2) web services, which offer four different cost models: on-demand, reserved instances, spot instances, and dedicated hosts. The on-demand cost model is the basic cost model, under which computing capacities are paid for by the hours without long-term commitments or upfront payments.

In this research, the on-demand cost model is employed to calculate the computation cost incurred during the clustering process:

\[
\text{Cost}_{\text{comp}} = \text{Price}_{\text{unit}} \times \text{Time}_{\text{comp}}
\]  

Computation time \(\text{Time}_{\text{comp}}\) is measured by the time taken by the clustering process. The unit price \(\text{Price}_{\text{unit}}\) is decided by the computational resource employed in running the algorithm. Take EC2 for example, there are seven major categories of EC2 VM instances: Linux, SLES, RHEL, windows, windows with SQL Standard, Windows with SQL Web and Windows with SQL Enterprise. In different categories, there are various types of EC2 VM instances available at different unit prices. For instance, in Windows category, 36 EC2 instances are displayed for 4 types: General Purpose, Compute Optimized, Memory Optimized, and Storage Optimized. The unit prices differ across different areas and range from $0.0066 to $38.054 per hour.

In this research, we use the computation time as an indicator of the computation cost for simplicity. When we use a specific Amazon EC2 VM instance, it can be found that the computation cost and computation time are positively correlated. Generally, the longer the computation time, the higher the computation cost is.

Before running the algorithms, some other costs may occur such as the transfer cost and storage cost of the big data set in the cloud. However, the costs incurred by data storage and data transfer are independent of the clustering process. Thus, in this research, we focus only on the cost incurred by the computation of the clustering process and isolate it from the other costs.

### 3.3 Cloud Computing Cost Model

The cost of computation resources when clustering big data can be calculated by the cost models offered by cloud vendors. In this research, we use Amazon’s Elastic Compute Cloud (Amazon EC2) web services, which offer four different cost models: on-demand, reserved instances, spot instances, and dedicated hosts. The on-demand cost model is the basic cost model, under which computing capacities are paid for by the hours without long-term commitments or upfront payments.

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### 3.4 Cost-effective Clustering Analysis

He et al. [7] demonstrated the long tail phenomenon using the k-means algorithm as an example. The same long tail phenomenon can also be found in our experiments using both k-means and EM algorithms (see Section 5), which makes it possible to compute and demonstrate the accuracy of the intermediate clustering result with incurred cost at each iteration of the clustering process.

In the clustering process, the long tail phenomenon is based on the convergence property of clustering algorithms. In the k-means algorithm, the objective function (sum of mean square of all points) is monotonically decreasing iteratively and can converge in finite steps. A rigorous proof of convergence property for k-means is given in [16]. For the EM algorithm, the objective function (log likelihood) is monotonically increasing and guaranteed to find a local maximum for the model parameters estimate [17]. From Fig. 3, we can see the change in the value of the objective function over computation time.
As the clustering process continues and the clustering results stabilize gradually, the convergence of k-means and EM become very slow, especially at the middle to late stage of clustering, which incur high costs for big data clustering. Fig. 3 shows the long tail phenomenon in the clustering process, where y-axis means the clustering accuracy calculated using Rand Index.

For the cost-effective clustering problem, the convergence rates of the objective functions for k-means and EM at a certain point can be analyzed with the clustering accuracy at the same time. This way, we can explore the relationship between them and propose a solution to cost-effective big data clustering in the cloud.

4 Proposed Approach for Big Data Clustering in the Cloud

In the k-means and EM clustering process, the objective function $J$ monotonically changes iteratively until converges in finite steps. For $i \in \{1, 2, ..., f\}$, the clustering partition $P_i$ is updated one iteration after another and gradually approaches the final result $P_f$, which means that the label of each point is updated iteratively and clustering accuracy $\text{Rand}(P_i, P_f)$ approaches 100%. Therefore, we set $r_i = \text{Rand}(P_i, P_f)$ to represent the clustering accuracy at the $i$th iteration.

The objective functions of k-means and EM algorithms are both monotonic and tend to converge over iterations [16], [17]. However, the value of objective function can be extremely dissimilar for different clustering algorithms (see Fig. 2) and can not be compared directly through the single value. Even with the same algorithm, the different distribution of data will lead to very distinct value of objective function. Therefore, in this research, we define the change rate of the value of the objective function at the $i$th iteration of the clustering process by $h_i$:

$$h_i = \frac{|J_i - J_{i-1}|}{|J_{i-1}|}, \quad i \in \{2, 3, ..., f\}$$

(7)

where $J_i$ indicates the value of the objective function at the $i$th iteration during the clustering process. As the clustering converges, the accuracy $r_i$ increases to 1 while $h_i$ decreases to 0. Therefore, there is a significant negative correlation between $h_i$ and $r_i$ (see Fig. 4).

In big data clustering, given a set of data points $D$, a random sampling strategy needs to be adopted first, and then the data set is partitioned into $n$ groups and each group has $k = D/n$ individuals. Random sampling is also called probability sampling, where each subject of $k$ individuals has the same probability of being chosen for the samples as other subjects of $k$ individuals [22]. Therefore, when the random sampling is done, each sample is an unbiased representation of the entire data and has the very same distribution pattern as other samples. After that, $n$ samples are split into training set and validation set.

In the training set, we utilize the regression analysis to develop a prediction model for estimating the relationship between $h_i$ and $r_i$ during the clustering process. The first concern is how to select the best regression model. In statistics, the sum squares due to error (SSE), R-square, adjusted R-square, and root mean squared error (RMSE) are commonly used as standard statistical metrics [23] for measuring the performance of the regression model. Generally, the closer the SSE and RMSE are to 0, the better the regression model selection and fitting, hence the more successful the data forecast. R-square and adjusted R-square range between 0 and 1, with a value closer to 1 indicating a better fit.

Based on comprehensive experiments, we found that the quadratic polynomial regression model shows the best fit than other popular regression models in most cases, such as linear regression, three-degree polynomial regression, exponential regression, logistic regression, lasso regression, etc. The quadratic polynomial model is as follows [24]:

$$h_i = \beta_0 + \beta_1 \times r_i + \beta_2 \times r_i^2 + \varepsilon, \quad i \in \{1, 2, ..., f\},$$

(8)

where $\varepsilon$ is an unobserved random error with mean zero conditioned on a scalar variable $\text{Rand}(i)$. $\beta_0, \beta_1, \beta_2$ are estimated parameters which represent the relationship between $h_i$ and $r_i$.

By establishing the regression model between these two variables in the training data set, we can estimate the changes in $h_i$ against the changes in $r_i$. Then, we conduct the clustering process iteratively in the validation data set when $h_i \leq h_j$. After that, we can terminate the clustering process to reduces unnecessary iterations and save computation costs.

To evaluate the proposed approach, we define the total computation time first. The total computation time $Time_{comp}$ includes the overall clustering time for the training data set $Time_{train}$, and the early-stop computation time $Time_{actual}$ when clustering reaches the desired accuracy, which can be calculated as:

$$Time_{comp} = Time_{train} + Time_{actual}$$

(9)

The training process is conducted only once. When it is finished, the regression model can be applied repeatedly for many applications. Thus, $Time_{train}$ is negligible compared to the overall cost in the long term (see Section 5.4 for the corresponding experimental analysis). Since computation time is the only indicator of the cost in our research, the cost effectiveness percentage $Cost_{effective}$ can also be represented as follows:

$$Cost_{effective} \approx \frac{Time_{actual}}{Time_{full}}$$

(10)
5 Experiment Result

In this section, we first describe the data sets and the experimental settings. Then, we evaluate the cost-effectiveness of the proposed approach. Finally, we discuss the performance of different clustering algorithms and illustrate the threats to validity.

5.1 Data Set Description

We have applied our approach to the 3D Road Network, Skin Segmentation, Poker Hand data sets from UCI machine learning repository and the SpaceNet data set of high-resolution satellite images from DigitalGlobe (see Table 1). The above data sets are the benchmarks for many studies in machine learning research and have been cited in high-impact peer-reviewed venues [25], [26], [27], [28].

The 3D Road Network data set has a total of 434,874 3-dimensional data points without class labels. It contains the longitude, latitude and altitude information about a road network covering a region of 185 × 135 km² in North Jutland, Denmark.

The Skin Segmentation data set has a total of 245,057 instances and is collected by randomly sampling B, G, R values from face images of various age groups, race groups and genders obtained from FERET database and PAL database. The data set is made up of 2 classes: the skin samples and non-skin samples.

The Poker Hand data set consists of 1,025,010 records and each record is an example of a hand consisting of five playing cards drawn from a standard deck of 52. Each card is described with two attributes (suit and rank), for a total of 10 predictive attributes. There is one attribute (class) that describes the “Poker Hand”.

The SpaceNet data set is an online repository of freely available satellite imagery collected from DigitalGlobe’s commercial satellites that includes more than 17,533 high-resolution images (438 × 406 pixels) in Rio De Janeiro, Las Vegas, Shanghai, and Khartoum areas. This data set contains a wealth of geospatial information relevant to many downstream use cases such as infrastructure mapping and land use classification.

5.2 Experimental Setup

Given the data sets at hand, the main purpose of the experimental setup is to use a default configuration on the parameters of the clustering algorithms. In general, finding an optimal number of clusters is an ill-posed problem of crucial relevance in clusters analysis [29]. Thus, we have chosen the number of clusters with respect to the number of unique class labels in the Skin Segmentation (2 classes) and the Poker Hand (10 classes) data sets. Since the 3D Road Network data set does not have class labels, we ran the data set with \( k = 4, 8 \). Usually, the number of clustering for remote sensing images is lower than 10 and can be set in required scenarios [30]. Thus, with the SpaceNet data set, we attempt to partition the images into six regions of pixels that can be given a common label, such as forest, water, road, building, grassland and wasteland for the land use classification as described in the motivating example, i.e., \( k = 6 \).

For non-image data sets, including the Skin Segmentation, the Poker Hand and the 3D Road Network data sets, a random sampling generation strategy was applied. In our research, for data set consisted of \( n \) points, we randomly select \( m \) data with \( n/m \) times. For example, for a data set consisted of 500,000 points, it can be divided into 20,000×25 (25 groups and each group has 20,000 points), 10,000×50, 5,000×100 etc. After extensive experiments, we found that when the data set has more groups and group size is larger (which means that we need to find a balance to make both of the groups number and size not too small), the experimental result usually shows better performance. Generally, when each group’s size is above 10,000 points and the number of groups is above 50, our approach achieves better results. The above phenomenon also indicates that the larger the data set, the more effective our method is. For SpaceNet imagery data set, since each satellite image has 438 × 406 data points, we regard each image as a sampling group for simplicity and there are 17,533 groups in total. Although the sampling size of SpaceNet data set is larger than the non-image data sets, this grouping strategy is still reasonable considering huge number of groups.

In the experiments, we use the 10-fold cross-validation to divide the groups into the training set and the validation set. For image data set (SpaceNet), each image is considered as a group. As the remote sensing data set is huge, we select 100 sample images as the training data set that can simulate the regression model quite accurately.

The experiments were implemented on Matlab r2013a and conducted on a machine with a 2.20 GHz Intel (R) Core (TM) i3 processor and 10G memory. The operating system is 64-bit Windows 7 enterprise.

5.3 Experimental Performance

In this section, we present and discuss the results achieved by the candidate clustering algorithms for the given data sets. Firstly, a data set sampling strategy is applied and the data sets are then divided into training data set and validation data set. We will introduce the experimental performance of our approach in the training process and validation process.

5.3.1 Training Process

Illustrating Long Tail Phenomenon. Fig. 5 shows the increase in the clustering accuracy over iterations during the clustering process for one group from the training set. Each
The EM algorithm as follows (see Fig. 6b):

This regression model illustrates the general relationship between the objective function $h_i$ calculated using (8) and clustering accuracy $r_i$ at the same iteration. In Fig. 6a, we see the relationship between $h_i$ and $r_i$ from all groups in the training data set (3D Road Network k = 4) by the k-means algorithm, which is represented by a series of scattered points. Then we can obtain the regression model by Matlab cftool box through the points using (8) as follows:

$$h_i = 1.83 \times r_i^2 - 3.66 \times r_i + 1.83$$

This regression model illustrates the general relationship between $h_i$ and $r_i$ in the k-means algorithm. Similarly, we obtain the regression model by the EM algorithm using (8) as follows (see Fig. 6b):

$$h_i = 0.007232 \times r_i^2 - 0.01479 \times r_i + 0.007558$$

Fig. 5. The clustering accuracy over computation time

Fig. 6. The regression model in training set (3D Network Road k=4)

marker on the curve indicates the intermediate partition at every iteration. It can be seen that the k-means algorithm first takes a relatively small number of iterations (19 iterations) to reach a high accuracy (95.06%), and then takes a large number of iterations (37 more iterations) to converge to the accuracy of 100%. This confirms the long tail phenomenon discussed in Section 3.3, which indicates that the majority of computation time is consumed at the middle to late stages. In our experiments, we also observed the long tail phenomenon with the different data sets using both k-means and EM, which indicates the feasibility of stopping at an early point of the clustering to achieve the desired accuracy.

In addition, fluctuations of accuracy may be observed in the early stage in clustering which is normal due to the chosen initial points. However, how to select the optimal initial points is not part of this research, so we do not discuss it in this paper.

Building Regression Model. We have explored the relationship between the change rate of the value of objective function $h_i$ calculated using (8) and clustering accuracy $r_i$ at the same iteration. In Fig. 6a, we see the relationships between $h_i$ and $r_i$ from all groups in the training data set (3D Road Network k = 4) by the k-means algorithm, which is represented by a series of scattered points. Then we can obtain the regression model by Matlab cftool box through the points using (8) as follows:

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$$h_i = 0.007232 \times r_i^2 - 0.01479 \times r_i + 0.007558$$

Table 2 The relation between accuracy and change rate of objective functions in k-means and EM

| Desired Accuracy | 90%        | 95%        | 99%        | 99.9%      |
|------------------|------------|------------|------------|------------|
| $h_i$ (k-means)  | 1.83e-2    | 4.60e-3    | 1.83e-4    | 1.83e-6    |
| $h_j$ (EM)       | 1.05e-4    | 3.44e-5    | 3.98e-6    | 3.33e-7    |

Setting Desired Accuracy. Then, we can set the desired accuracy $r_j$ and calculate the corresponding $h_j$ through the regression model obtained from the training process. Here, due to the page limit, we only consider the situations when desired accuracies are set for $r_j = 90\%, 95\%, 99\%$ and $99.9\%$ which we believe are sufficient. Table 2 displays the relationship between the desired accuracy and change rate of the value of the objective function intuitively in 3D Road Network data set when $k = 4$.

The candidate clustering algorithms are terminated in the iterative process once the change rate of the objective function $h_i$ is below the set value $h_j$, i.e., $h_i \leq h_j$. In a real-world application, the clustering task will stop when it reaches the desired accuracy.

5.3.2 Validation Process

To validate the performance of the proposed approach, we mainly focus on two aspects: cost effectiveness and achieved accuracy.

Cost-effectiveness Validation. We run validation set for different data sets and obtain the total clustering completion time $Time_{full}$ for k-means and EM algorithms. Fig. 7 shows the percentages of actual computation time $Time_{actual}$ by using our approach in different data sets. By setting the desired accuracy, the candidate algorithms can stop at an early point. After using Eq. (10), the average actual computation time is only at $23.74\%$, $33.50\%$, $56.57\%$ and $81.06\%$ of the total time when desired accuracies are $90\%$, $95\%$, $99\%$, and $99.9\%$ respectively using the k-means algorithm. Similarly, for EM algorithm, the average actual computation time accounts for $9.4\%$, $14.46\%$, $20.73\%$, and $32.78\%$ respectively of the total computation time. Since the cloud computation cost is directly related to computation time, both k-means and EM algorithms can achieve high cost effectiveness in the clustering process in the cloud using our approach.

Achieved Accuracy Validation. In the experiment, we record the expected stop point for different desired accuracies and calculate the real achieved accuracies. From Table 3 and Table 4, we can see that the average achieved accuracies are $92.09\%$, $95.47\%$, $98.50\%$ and $99.81\%$ when corresponding desired accuracies are $90\%$, $95\%$, $99\%$, and $99.9\%$ respectively for the k-means algorithm. Similarly, for the EM algorithm, the average achieved accuracies are $90.24\%$, $96.08\%$, $99.11\%$ and $99.76\%$ respectively with the same desired accuracy. The numbers in parentheses represent the standard deviations that are generated by different groups for the data set in the clustering process. Fig. 8a and Fig. 8b are the box plots of desired accuracy and achieved accuracy in one group of SpaceNet validation set. It clearly shows that the average of actual achieved accuracy is very close to the desired accuracy for both algorithms. The standard deviation is small especially when desired accuracy reaches $99\%$ and $99.9\%$. 

TABLE 2

| Desired Accuracy | 90%        | 95%        | 99%        | 99.9%      |
|------------------|------------|------------|------------|------------|
| $h_i$ (k-means)  | 1.83e-2    | 4.60e-3    | 1.83e-4    | 1.83e-6    |
| $h_j$ (EM)       | 1.05e-4    | 3.44e-5    | 3.98e-6    | 3.33e-7    |
### TABLE 3
Achieved accuracy for K-means

| Dataset / k | Desired Accuracy (Standard Deviation) |
|-------------|---------------------------------------|
|             | >90%        | >95%        | >99%        | >99.9%       |
| 3D_Road / 4 | 91.67% (0.1670) | 95.84% (0.0094) | 99.14% (0.0040) | 99.93% (0.0015) |
| 3D_Road / 8 | 90.92% (0.0207) | 94.33% (0.0278) | 97.78% (0.0226) | 99.77% (0.0059) |
| Skin_Seg / 2 | 91.79% (0.0068) | 96.86% (0.0050) | 98.87% (0.0036) | 99.75% (0.0013) |
| Poker_Hand / 10 | 94.00% (0.0235) | 95.58% (0.0240) | 98.09% (0.0211) | 99.80% (0.0061) |
| SpaceNet / 6 | 92.05% (0.0349) | 94.75% (0.0341) | 98.64% (0.0098) | 99.79% (0.0036) |
| **Average**  | 92.09%       | 95.47%       | 98.50%       | 99.81%       |

### TABLE 4
Achieved accuracy for EM

| Dataset / k | Desired Accuracy (Standard Deviation) |
|-------------|---------------------------------------|
|             | >90%        | >95%        | >99%        | >99.9%       |
| 3D_Road / 4 | 90.71% (0.1599) | 95.16% (0.0551) | 98.07% (0.0310) | 99.63% (0.0015) |
| 3D_Road / 8 | 91.67% (0.0467) | 95.84% (0.0094) | 99.14% (0.0040) | 99.93% (0.0015) |
| Skin_Seg / 2 | 91.15% (0.1138) | 99.93% (0.0004) | 99.97% (0.0003) | 99.99% (0.0002) |
| Poker_Hand / 10 | 88.53% (0.0711) | 94.67% (0.0505) | 98.17% (0.0297) | 99.31% (0.0168) |
| SpaceNet / 6 | 89.12% (0.0492) | 94.81% (0.0384) | 99.24% (0.0181) | 99.95% (0.0006) |
| **Average**  | 90.24%       | 96.08%       | 99.11%       | 99.76%       |

#### Fig. 7
The percentage of computation time with different desired accuracies by using k-means and EM

#### Fig. 8
The box plots of desired accuracy and achieved accuracy
which proves the high precision of the quadratic polynomial regression in the experiment. When required accuracy is 90% and 95%, the achieved accuracy of EM algorithm has larger variation than that of k-means algorithm, which means k-means has better goodness of fit of the regression model than EM algorithm (corresponding to Fig. 3). To sum up, k-means is more stable in achieved accuracy than EM in which more anomalies and larger variation can be observed.

5.5 Threats to Validity

In this section, some key threats to the validity will be discussed as follows.

Threats to construct validity. The main threat to the construct validity is the adopted metric to evaluate the accuracy of every intermediate partition during the clustering iterative process. In the paper, we use the Rand Index as the adopted metric. As introduced in Section 3.2, the Rand Index relies on the final partition in the clustering and it is an external clustering index. In most clustering algorithms, the evaluation criteria are divided into internal and external clustering indices. The internal evaluation criterion is to evaluate the goodness of a data partition without prior knowledge from the data sets, which includes Compactness (CP), Separation (SP), Davies-Bouldin Index (DB), Dunn Validity Index (DVI), etc. And the external evaluation criterion is to assess how accurately a clustering technique partitions the data relative to their correct class labels. In real-world clustering, it is difficult and impractical to retrieve the correct class labels. Thus, the Rand Index is not the usual choice for the real-world big data clustering. However, this threat to validity is minimal because our objective is to explore and demonstrate how to stop a clustering process at some point to achieve high cost-effectiveness. The Rand Index can accurately evaluate how close an intermediate partition to the final partition in the training process while internal indices might not be consistently correlated with Rand Index.

Threats to conclusion validity. The central threat to the conclusion validity is the reliability of the final partition of the clustering iterative process as the optimal partition. Since the k-means and EM algorithms do not guarantee a global optimum, they attempt to approximate the optimal partition. Therefore, the final partition of the clustering result is not necessarily the optimal partition. So, Fig. 3 do not necessarily demonstrate how the intermediate partition approaches the real optimal partition. Nevertheless, we are able to consider the final partition adequately reliable for demonstrating the long tail phenomenon in the clustering process because in the optimal situations, the k-means and EM algorithms are likely to take more time and result in a more significant long tail phenomenon. Thus, the threat to the conclusion validity exists but is not significant.

Threats to external validity. The main threat to the external validity in our research is the representativeness of the data sets used in the experiments. In the experiments, we used the 3D Road Network, Skin Segmentation, Poker Hand and SpaceNet data sets. All the data sets are real-world data sets. They may have their own characteristics and thus do not comprehensively present all data sets. However, the main features are familiar such as the negative relationship between change rate of the value of the objective function and the clustering accuracy. In the meantime, the high cost-effectiveness and small standard deviation in all given data sets indicate that the threat to the external validity is minimal.

Threats to internal validity. The crucial threat to internal validity is the selection of the regression model. In the experiments, we found that the quadratic polynomial regression model shows the best result of R-squared and SSE for all given data sets. However, it is impossible to exhaust every data set in the real world to ensure if the quadratic polynomial model is the best regression model. For instance, the regression model may be one degree, three-
degree polynomial models or even non-polynomial model such as the exponential model in some special data sets. Nevertheless, different types of regression models can also be applied in our approach to achieve cost-effectiveness for the big data clustering in the cloud. Thus, the threat to the internal validity is minimal.

6 Related Work

With the development of the pay-as-you-go model, the IT resources are usually provisioned and utilized by cloud computing. Since the majority of advantages offered by cloud computing are built around the flexibility of the pay-as-you-go cost model, cost-effectiveness has become a critical issue in cloud computing filed. With the improving cloud services from the cloud vendors, many scientists focus on the performance as well as cost-effectiveness of public cloud services. Intensive research work has been made on the cost-effective computation in the cloud environment. A Semi-Elastic Cluster (SEC) computing model [32] has been proposed for organizations to reserve and dynamically resize a virtual cloud-based cluster. The race-driven results show that such a model has a 61% percent cost saving than individual users acquiring and managing cloud resources without causing longer average job wait time. And a new MapReduce cloud service model Cura was presented to provide a cost-effective solution to efficiently handle MapReduce production resources, which implemented a globally efficient resource allocation scheme that significantly reduces the resource usage cost in the cloud. A new task scheduler Flutter [33], was designed and implemented which reduces both the completion time and network cost of big data processing jobs across geographically distributed data centers.

Cost-effectiveness of scientific computing applications has also been studied by Berriman et al. using Amazons EC2 [34]. They compared Amazons EC2 with the Abe high-performance cluster and drew the conclusion that the Amazon EC2 offers better performance and value for processor- and memory-limited applications than for I/O-bound applications. A similar study was conducted by Carlyles team to compare the computation cost of high-performance in traditional HPC environments and in Amazons EC2 environments, using Purdue Universitys HPC community cluster program [35]. Their research showed that an in-house cluster is more cost-effective when the organization having sufficient demand that fully utilizes the cluster or having an IT department capable of sustaining IT infrastructure or having cyber-enabled research as a priority. These features of in-house clusters, in fact confirm the flexibility and cost effectiveness of running computation-intensive applications in the commercial clouds. Wang et al. proposed a stochastic multi-tenant framework for investigating the response time of cloud services as a stochastic metric with a general probability distribution [36]. In a similar study, by comparing between the scaling out strategies with the scaling up strategies, the performance of Amazons cloud services was tested with five benchmark applications and scaling up is found more cost-effective in sustaining heavier workload [37]. To find the minimum cost of storing and regenerating datasets in multiple clouds, a novel algorithm was proposed which achieved the best trade-off among computation, storage and bandwidth cost in the cloud [38]. Jawad et al. [39] proposed a smart power management system to minimize the operation cost of data center, which coordinates the data center workload, diesel generators, battery bank, renewable power, real-time trade electricity price and day-ahead power market to reduce consumption cost.

The current research for cloud computing shows the popularity of running computation-intensive applications in the cloud, which describes a general overview about cost effectiveness for big data clustering in the cloud through a comparison between the cloud environment and a traditional cluster environment. Additionally, to save cost in the cloud, it is also critical for clustering algorithms to improve their efficiency and to reduce processing time. To deal with the problem, many approaches have been proposed. To optimize the k-means algorithm, how to select k appropriate initial centers is a key issue and there have been many pieces of work on this matter [40], [41], [42]. For the EM algorithm, Liu et al. used the parameter expansion to accelerate EM [43]. However, such approaches rarely considered the economic efficiency. Up until now, none of the existing research has considered the k-means or EM algorithm from the cost-effective perspective about cost-effective big data clustering in the cloud. He et al. found the phenomenon that achieving 99% accuracy of k-means only needs an average of 20%+ of the total computation time [7], but they did not offer a solution for terminating the clustering algorithm at an early point with the desired accuracy.

In our research, from a different and important perspective, we take a look at the issue of cost-effectiveness how to achieve a sufficiently satisfactory accuracy at a relatively small proportion of the total cost of achieving 100% accuracy by stopping the clustering process at an early point before its completion.

7 Conclusion and Future Work

In this research, we proposed a novel approach for cutting the unnecessary long tail to achieve cost-effective big data clustering in the cloud. Users can achieve sufficiently satisfactory accuracies at the lowest possible costs by setting their desired accuracies. With our approach, both widely used k-means and EM algorithms show high cost effectiveness in the clustering process. For the k-means algorithm, achieving 99% accuracy only needs 47.71%-71.14% of the computation time for achieving a 100% accuracy. And for the EM algorithm, achieving a 99% accuracy needs 16.69%-32.04%. By applying our proposed approach, the government will save up to $94, 687.49 for the United States land use statistics for each run.

To the best of our knowledge, this is the very first paper to achieve cost effectiveness for big data clustering in the cloud by cutting the unnecessary long tail. This work presents a significant first step toward cost-effective clustering in the cloud. As a contribution, our approach can be easily deployed in various fields which need to clustering big data with limited budget.

Since k-means and EM algorithms may not be suitable for time-series data and spatiotemporal data, in the future,
we plan to investigate the cost effectiveness of the clustering algorithms for those data types. In addition, it is also valuable to explore the relationship between the achieved accuracy and acquired accuracy, and control the margin of error by artificial setting.

ACKNOWLEDGMENTS

The work is partly funded by the China Scholarship Council.

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APPENDIX A

The notations used in this paper are shown in Table A.1.

| Notation | Definition |
|----------|-----------|
| $D$      | A given data set to be partitioned |
| $x$      | A feature point with dimensions |
| $k$      | The number of clusters |
| $n$      | The number of iterations in the clustering process |
| $c_i$, $c_j$ | The cluster centers |
| $C$      | The cluster centers set |
| $C_i$    | The set of data points that are closer to $c_i$ than to $c_j$ for all $j \neq i$ |
| $P_i$    | The clustering partition at the $i$th iteration. |
| $\text{Rand}(P_i, P_j)$ | The rand index of two partitions $P_i, P_j$ |
| $r_i, r_j$ | The clustering accuracy at the $i$th iteration |
| $J$      | The objective function of clustering algorithm |
| $J_i$    | The value of the objective function at the $i$th iteration |
| $h_i, h_j$ | The change rate of objective function at the $i, j$th iteration |
| $\text{Time}_{\text{comp}}$ | The total computation time |
| $\text{Time}_{\text{train}}$ | The computation time for training |
| $\text{Time}_{\text{actual}}$ | The computation time when accuracy reaches users desired accuracy |
| $\text{Time}_{\text{full}}$ | The computation time when clustering reaches 100% accuracy |
| $\text{Cost_{effective}}$ | The cost effectiveness percentage |

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