SELF-CONSISTENT MODEL ATMOSPHERES AND THE COOLING OF THE SOLAR SYSTEM’S GIANT PLANETS

J. J. Fortney\textsuperscript{1,5}, M. Ikoma\textsuperscript{2}, N. Nettelmann\textsuperscript{1}, T. Guillot\textsuperscript{3}, and M. S. Marley\textsuperscript{4}

\textsuperscript{1}Department of Astronomy and Astrophysics, University of California, Santa Cruz, CA 95064, USA; jfortney@ucolick.org
\textsuperscript{2}Department of Earth and Planetary Sciences, Tokyo Institute of Technology, Ookayama, Meguro-ku, Tokyo 152-8551, Japan
\textsuperscript{3}Observatoire de la Côte d’Azur, Laboratoire Cassiopeée, CNRS UMR 6202, BP 4229, 06304 Nice Cedex 4, France
\textsuperscript{4}Space Science and Astrobiology Division, NASA Ames Research Center, Mail Stop 245-3, Moffett Field, CA 94035, USA

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ABSTRACT

We compute grids of radiative–convective model atmospheres for Jupiter, Saturn, Uranus, and Neptune over a range of intrinsic fluxes and surface gravities. The atmosphere grids serve as an upper boundary condition for models of the thermal evolution of the planets. Unlike previous work, we customize these grids for the specific properties of each planet, including the appropriate chemical abundances and incident fluxes as a function of solar system age. Using these grids, we compute new models of the thermal evolution of the major planets in an attempt to match their measured luminosities at their known ages. Compared to previous work, we find longer cooling times, predominantly due to higher atmospheric opacity at young ages. For all planets, we employ simple "standard" cooling models that feature adiabatic temperature gradients in the interior H/He and water layers, and an initially hot starting point for the calculation of subsequent cooling. For Jupiter, we find a model cooling age \( \sim 10\% \) longer than previous work, a modest quantitative difference. This may indicate that the hydrogen equation of state used here overestimates the temperatures in the deep interior of the planet. For Saturn, we find a model cooling age \( \sim 20\% \) longer than previous work. However, an additional energy source, such as that due to helium phase separation, is still clearly needed. For Neptune, unlike in work from the 1980s and 1990s, we match the measured \( T_{\text{eq}} \) of the planet with a model that also matches the planet’s current gravity field constraints. This is predominantly due to advances in the high-pressure equation of state of water. This may indicate that the planet possesses no barriers to efficient convection in its deep interior. However, for Uranus, our models exacerbate the well-known problem that Uranus is far cooler than calculations predict, which could imply strong barriers to interior convective cooling. The atmosphere grids are published here as tables, so that they may be used by the wider community.

Key words: planets and satellites: atmospheres – planets and satellites: individual (Jupiter, Saturn, Uranus, Neptune) – planets and satellites: interiors

Online-only material: color figures

1. INTRODUCTION

Planets cool as they age. For giant planets, what regulates the cooling of their mostly convective interiors is the radiative properties of the thin skin of atmosphere that rests atop the bulk of the planet’s mass. The effect of atmospheres on giant planet cooling was first investigated in the mid-1970s, when Graboske et al. (1975), Hubbard (1977), and Pollack et al. (1977) computed the first thermal evolution models of Jupiter and Saturn that coupled the atmospheric and interior structures. The relationship between the atmosphere and interior has become even better appreciated since the discovery of hot Jupiters 15 years ago (Mayor & Queloz 1995), which orbit their parent stars at 5–10 stellar radii and often intercept \( 10^9–10^{10} \) more flux than Jupiter receives from the Sun. This incident flux drives the external radiative zone to pressures near 1 kbar in Gyr-old planets (Guillot et al. 1996; Sudarsky et al. 2003; Fortney et al. 2007), which suppresses the transfer of intrinsic flux through the atmosphere, thereby slowing interior cooling and contraction. A great variety of model atmosphere grids have been calculated for these close-in planets (e.g., Burrows et al. 2003; Baraffe et al. 2003, 2008; Fortney et al. 2007; Ibgui & Burrows 2009), which feature state-of-the-art treatments of chemistry (e.g., Lodders & Fegley 2006), non-gray opacities (e.g., Sharp & Burrows 2007; Freedman et al. 2008), and radiative transfer.

These same atmosphere models have been honed over the past 10 years on excellent spectra of hundreds of brown dwarfs with \( T_{\text{eff}} \) down to \( \sim 550 \) K (Allard et al. 2001; Marley et al. 2002; Burrows et al. 2006; Saumon et al. 2006; Saumon & Marley 2008). But these tools have not been applied to generate modern model atmosphere grids for use in evolution models of the solar system’s giant planets.

The first and last grids of non-gray radiative–convective model atmospheres to be tabulated in print for use in evolutionary calculations were presented in Graboske et al. (1975). These were computed for planetary effective temperatures of 20–1900 K, at only two surface gravities, that of the current Jupiter and at 1/64 Jupiter’s current gravity. More recently, Burrows et al. (1997) and Baraffe et al. (2003) computed non-gray atmosphere models for use in the evolution of brown dwarfs and giant planets, including Jupiter and Saturn (Hubbard et al. 1999; Fortney & Hubbard 2003), but these grids are not available to the wider community. Both Graboske et al. (1975) and Burrows et al. (1997) did not treat irradiation from the Sun.

The purpose of this paper is to provide radiative–convective atmosphere grids for Jupiter, Saturn, Uranus, and Neptune, for the full ranges of surface gravities, effective temperatures, incident fluxes, and atmospheric compositions specific to these planets, as a function of planet age. This will greatly minimize any remaining uncertainty in cooling calculations related to the atmospheric boundary condition for these planets. Here
we also apply these grids to investigate what effect they have on the cooling histories of the planets.

We can briefly summarize the main findings of evolution models of the major planets.\(^6\) Going back to Hubbard (1977), evolution models of Jupiter have yielded a planetary \(T_{\text{eff}}\) roughly consistent with observations at an age of 4.6 Gyr, under the assumption of a fully adiabatic interior (Hubbard et al. 1999; Fortney & Hubbard 2003), or with a small radiative zone (Guillot et al. 1995). These models use an initial, post-formation \(T_{\text{eq}}\) that is arbitrarily large (see, e.g., Marley et al. 2007a), on the order of 1000 K, implying that Jupiter was quite luminous at young ages, as is expected from any model of its formation. Jupiter’s evolution is considered fairly well understood.

Fully convective homogeneous models of Saturn reach the planet’s known \(T_{\text{eff}}\) in only 2–3 Gyr, implying that Saturn is much warmer than can be accommodated by the same kind of model that works well for Jupiter (Pollack et al. 1977). The phase separation of helium from liquid metallic hydrogen, and its subsequent sinking to deeper layers (a differentiation process), has long been suspected of providing Saturn’s additional energy source (Salpeter 1973; Stevenson 1975; Stevenson & Salpeter 1977a, 1977b). While this is widely assumed to be true, the exact details of the physics (Morales et al. 2009; Lorenzen et al. 2009) and its implementation in cooling models (Hubbard et al. 1999; Fortney & Hubbard 2003) have not yet been solved.

Uranus and Neptune cooling models have their own problems, which are different from those of Jupiter and Saturn. Hubbard (1978) and Hubbard & Macfarlane (1980) computed the first thermal evolution models of these planets. Hubbard & Macfarlane (1980) could only find good agreement between model cooling ages and the age of the solar system if the planets started out relatively cool, with post-formation values of \(T_{\text{eff}}\) only \(\sim 50\%\) greater than their current values. Put another way, the current planets were found to be underluminous compared to models that started with the arbitrarily large initial \(T_{\text{eff}}\) values used for Jupiter and Saturn. The problem was especially pronounced for Uranus.

Later work on cooling models can be found in Podolak et al. (1991) and Hubbard et al. (1995). Again, both Uranus and Neptune appeared underluminous compared to models, although the discrepancy was larger for Uranus than for Neptune. Podolak et al. (1991) hypothesized that statically stable layers in the interior of the “ice giants,” due to compositional layering, could lock in internal energy, leading to small intrinsic fluxes. They suggested that only the outer 40% and 60% in radius of Uranus and Neptune, respectively, were freely convecting. It is known that the interior structures of these planets do not need to be partitioned into well-defined layers (Marley et al. 1995). More recently, and importantly, Fortney & Nettelmann (2010) computed new cooling models of these planets. They used a new water equation of state (EOS; French et al. 2009), and find that Neptune’s current \(T_{\text{eff}}\) can be matched, while the problem with Uranus remains, for models that feature the standard arbitrary hot start. The implication is that the argument for stable layers in Neptune may no longer be necessary.

To summarize, current state-of-the-art models can reproduce the \(T_{\text{eff}}\) of Jupiter and Neptune, while Saturn is overluminous and Uranus is underluminous. In this paper, in Section 2 we describe new model atmospheres for all of these planets, and apply them to new cooling models in Section 3. In Section 4, we give our conclusions and suggest future work.

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\(^6\) A nice review of work until 1980, the early years of giant planet spacecraft observations and evolution modeling, can be found in Hubbard (1980).
directly adds to the energy budget of the planet (Hubbard 1977; Fortney & Hubbard 2003). Given that all the giant planets have stratospheres, due to absorption of incident flux in the radiative atmosphere, this assumption does not hold. In addition, one must assume a Bond albedo at every age, in order to determine the amount of absorbed incident flux. Typically, the current Bond albedo is used at all ages. Here, we consistently solve for the deposition of stellar flux into the atmosphere as a function of wavelength and depth, and make no assumption regarding the Bond albedos. The \( T_{\text{eff}} \) at a given \( T_0 \) and \( g \) is obtained based on the converged radiative–convective equilibrium model atmosphere temperature/pressure/opacity profile.\(^7\) As mentioned above, this improved method of treating the atmospheric boundary has been used for the close-in “hot Jupiter” planets for several years (see, e.g., Baraffe et al. 2003; Burrows et al. 2003, for initial calculations) and was extended by Fortney et al. (2007) to models of extrasolar giant planet thermal evolution for planets from 0.02 to 10 AU.

Here, the derived pressure–temperature \((P–T)\) profiles are for planet-wide average conditions, with a sunlight zenith angle of 60 deg \((\mu = 0.5)\), and the incident flux cut by 1/2, due to the day/night difference (Marley & McKay 1999). Using an analytical model for a semi-gray, non-scattering atmosphere (Guillot 2010), we compared solutions obtained with that approximation to globally averaged solutions, with a greenhouse factor \((i.e., the ratio of the infrared to the visible mean opacities)\) between 10–2 and 100. We found that mean deviations in the temperature profile between optical depths \( \tau = 10^{-2} \) and 100 were smaller than 1.4%, with a standard deviation smaller than 3.2%, i.e., much smaller than other uncertainties.

While the model atmospheres presented here are a significant advance over previous calculations, some simplifications are still made. Most importantly, we neglect the opacity of condensate clouds and non-equilibrium hazes. For instance, the geometric albedos of Jupiter and Saturn are depressed in the blue due to dark hazes (Karkoschka 1994) that are thought to be derived from the photochemical destruction of methane (Rages et al. 1999). However, to our knowledge there is no adequate theory to predict how the optical depth and distribution of this haze may change as a function of solar luminosity, planetary \( T_{\text{eff}} \), and chemical mixing ratios, which change as the planets cool. Even more importantly, equilibrium condensate clouds such as water or ammonia lead to large geometric albedos outside of methane absorption bands (e.g., Cahoy et al. 2010). However, the cloud optical properties, particle sizes, vertical distribution, and coverage fraction are difficult or impossible to predict from first principles. See Ackerman & Marley (2001), Cooper et al. (2003), and Helling & Woite (2006) for modern cloud models for substellar objects.

Of significant practical importance, and what validates our cloud-free assumption here, is that we reproduce the current temperature structure and \( T_{\text{eff}} \) of the Jovian atmosphere much better with cloud-free models than with models that include ammonia and water clouds (Cahoy et al. 2010). The cloudy models (which use the Ackerman & Marley cloud model) yield model atmospheres that are too reflective (a high Bond albedo) and are, hence, too cool. This is because without dark photochemical hazes, the ammonia and water condensate clouds in the atmosphere model are more reflective than observed. Cloud layers in Uranus and Neptune reside deeper in the atmosphere, which makes this issue less important for their atmospheres. Looking back in time, when the planets will be warmer, points to a proper treatment of the time-varying Bond albedos being a very complicated problem. The cloud layers in Uranus and Neptune will be higher in the atmosphere. Jupiter and Saturn will lose their ammonia clouds and possess a top layer of thick water clouds. There is much future work to be done in this area.

Fortunately, for Jupiter and Saturn, the neglect of both the dark absorbing hazes, and relatively bright condensate clouds somewhat cancel out, and we are able to reproduce the temperature structure of the planets’ tropospheres quite well. The example of a cloud-free model of the current Jupiter, compared to data from the Galileo Entry Probe (Seiff et al. 1998), is shown in Figure 1. The model \( T_{\text{eff}} \) is correct to 0.2 K, and the 1 bar temperature (within the convective region) to 4 K. In Figure 2 we show a comparison with the atmosphere of Neptune, which was probed via radio occultation by Voyager 2 (Lindal 1992). The comparison here is also favorable, with differences only on the order of several degrees. Since these planets cool very slowly at gigayear ages, a good match to \( T_{\text{eff}} \) and \( T_{10} \) now also indicates a good match for the past several gigayears.

\[ T_0 = Kg^{-0.167}T_{\text{eff}}^{1.423}, \]  

where \( T_0 \) is the temperature at a reference pressure \( P_0 \) within the convective region of the atmosphere, such as 1 or 10 bars, and \( K \) is a constant. Saumon et al. (1996) find that \( T_0 = 10 \) bar and \( K = 3.36 \) provides a reasonable fit below \( T_{\text{eff}} \) of 200 K. For Uranus

\(^7\) The Bond albedo cannot be precisely determined from a one-dimensional model. A multi-dimensional model must be used to investigate the scattering of light over all phase angles (e.g., Marley & McKay 1999; Cahoy et al. 2010).
and Neptune evolution models, Hubbard & Macfarlane (1980), in order to better match the planet’s atmospheres, suppressed the gravity dependence entirely and set $K = 1$, with $P_0 = 0.750$ bar for Uranus, and $P_0 = 0.861$. So, in general, a variety of fits, some based on the original calculations, some based on ad hoc modifications, are available. Clearly new work in this area is warranted.

The Burrows et al. (1997) grid, slightly updated in Hubbard et al. (1999), spans a very wide range of $T_{\text{eff}}$, $g$, and $T_{10}$, with a mix of gray atmospheres at high $T_{\text{eff}}$, and non-gray atmospheres at low $T_{\text{eff}}$, suitable for giant planets. The Baraffe et al. (2003) grid, fully non-gray, is similarly expansive, to treat the lowest mass stars, brown dwarfs, and planets.

We have computed $P-T$ profiles for Jupiter and Saturn at $\sim 50$ $T_{\text{eff}}/g$ pairs, enough for detailed coverage of the evolution of $T_{\text{int}}$, $g$, and $S$, over their evolution. For Jupiter, $T_{\text{int}}$ ranges from 89 K to 1200 K, while the gravity range covers 0.12 to 1.1 $\times$ Jupiter’s gravity. For Saturn, $T_{\text{int}}$ ranges from 69 K to 650 K, while the gravity range covers 0.12 to 1.1 $\times$ Saturn’s gravity. For both planets, these calculations were done at the current value of the incident solar flux, as well as 0.7 of this value so that the evolution of the solar luminosity can be incorporated (e.g., Hubbard et al. 1999). These are included as Tables 1 and 2, for Jupiter and Saturn, respectively. The grids for 1.0 $L_\odot$ for Jupiter and Saturn are shown in Figures 3 and 4, respectively. They show $T_{\text{int}}$ and $T_{\text{eff}}$ on the x-axis, and $T_{10}$ on the y-axis, for eight different surface gravities. Low gravities cover high $T_{\text{int}}$ (young ages) and high gravities cover low $T_{\text{int}}$ (old ages).

An inset shows $T_{\text{int}}$ versus $T_{\text{eff}}$ for the current and lower solar luminosity, at very low $T_{\text{eff}}$. When $T_{\text{int}}$ is large, then the planet’s energy budget is dominated by its own intrinsic luminosity, and $T_{\text{int}}$ is only negligibly larger than $T_{\text{int}}$. However, at lower values of $T_{\text{int}}$, eventually there is a clear separation between $T_{\text{int}}$ and $T_{\text{eff}}$, as expected.

For Uranus and Neptune, we have computed four separate grids, at four different values of the incident flux. The $T_{\text{int}}$ ranges

### Table 1

| Gravity | $T_{\text{eff}}$, 1.0 | $T_{10}$, 1.0 | $T_{\text{eff}}$, 0.7 | $T_{10}$, 0.7 | $T_{\text{int}}$ |
|---------|---------------------|---------------|---------------------|---------------|-----------------|
| 3.2     | 1201.6              | 3471.1        | 1201.6              | 3471.1        | 1200            |
|         | 904.7               | 3124.9        | 904.7               | 3124.9        | 900             |
|         | 751.3               | 2894.2        | 751.2               | 2894.2        | 750             |
|         | 600.6               | 2582.3        | 600.5               | 2582.4        | 600             |
| ...     | ...                 | ...           | ...                 | ...           | ...             |
| 5.6     | 1201.2              | 3359.3        | 1202.6              | 3360.3        | 1200            |
| ...     | ...                 | ...           | ...                 | ...           | ...             |
| 9.1     | 1201.8              | 3255.1        | 1202.2              | 3255.8        | 1200            |
|         | 901.5               | 2850.3        | 901.5               | 2850.2        | 900             |
|         | 750.5               | 2571.4        | 750.5               | 2571.4        | 750             |
|         | 600.4               | 2222.1        | 600.3               | 2222.1        | 600             |
|         | 450.6               | 1816.0        | 450.4               | 1815.9        | 450             |
| ...     | ...                 | ...           | ...                 | ...           | ...             |
| 13.5    | 1201.5              | 3165.6        | 1201.8              | 3166.0        | 1200            |
| ...     | ...                 | ...           | ...                 | ...           | ...             |
| 18.2    | 1201.7              | 3030.5        | 1201.8              | 3030.5        | 1200            |
|         | 750.3               | 2330.5        | 750.3               | 2330.5        | 750             |
|         | 600.3               | 1987.6        | 600.2               | 1987.6        | 600             |
|         | 450.6               | 1617.7        | 450.4               | 1617.6        | 450             |
| ...     | ...                 | ...           | ...                 | ...           | ...             |

The model parameters are shown on the plot. The value of $T_{\text{int}}$ is chosen to match the value of the intrinsic flux measured by Voyager 2. The resulting $T_{\text{int}}$ is 59.2 K, the observed value within the observational error bars. The model planet’s 1 bar temperature is warmer by 5 K than that measured by Voyager 2. Extrapolating to the 10 bar level, the temperature appears to be a good match.
from 27 to 217 K, while the gravity range covers 0.45 × Uranus’ gravity to 1.1 × Neptune’s gravity. Two values of the incident flux are for the current values for Uranus and Neptune, at 19.2 and 30.1 AU from the current Sun, respectively. The other two are at 1.8 × the current flux received by Uranus, and 0.12 × the current flux received by Neptune. This very wide range allows for the inclusion of a time variable solar luminosity as well as the possibility of dramatic changes in the orbital distances of the planets with time (e.g., Gomes et al. 2005). The grids at Uranus’ and Neptune’s current flux levels are compiled in Table 3 and shown in Figures 5 and 6, respectively. At high $T_{\text{eff}}$, the two grids appear quite similar, but for Uranus’ larger incident flux, the wider division between $T_{\text{int}}$ and $T_{\text{eff}}$ at low $T_{\text{int}}$, is readily apparent. For nearly all models of the four planets, the atmosphere becomes convective and stays convective by 10 bars. For a handful of models for Jupiter, the deep convective adiabat was not reached until ~15 bars, but the tabulated value of $T_{10}$ is modified to be consistent with the entropy of the deep adiabat (see Burrows et al. 1997).

The model atmosphere grid, and its relation between $S$, $T_{\text{int}}$, and $T_{\text{eff}}$, comes in through the energy conservation equation:

$$\frac{dL}{dm} = -T \frac{dS}{dt},$$  

(2)

where $L$ is the luminosity, $m$ is the mass variable, $T$ is the temperature in a mass shell, $S$ is the specific entropy of that shell, and $t$ is the time. After explicitly defining the dimensionless mass
shell variable \(m\) as

\[ m = \frac{1}{M} \int_0^r 4\pi r^2 dr' \rho(r'), \]  

we can rewrite Equation (2) in terms of the time step \(\partial t\), as

\[ \partial t = -\frac{M}{L} \int_0^1 T \partial S dm, \]  

where \(\partial t\) is the time step between two models that differ in entropy by \(\partial S\). The luminosity \(L\) extracted from the planet is \(4\pi R^2 \sigma T_{\text{int}}^4\), where the value of \(T_{\text{int}}\) at a given \(S\) is given by the model atmospheres. While at young ages \(T_{\text{int}} \sim T_{\text{eff}}\), at old ages, when \(T_{\text{int}}\) can be appreciably smaller than \(T_{\text{eff}}\), interior cooling can be quite slow. After presenting our new cooling calculations in the next section, in Section 3.3 we will examine the affects of the new atmosphere grids, compared to previous tabulations.

### 3. COOLING CALCULATIONS

#### 3.1. Jupiter and Saturn

Using these new model atmosphere grids, we can calculate the cooling history of the major planets. Cooling calculations for these planets have been published by many authors. Recent work for Jupiter and Saturn includes Hubbard et al. (1999), who explicitly showed the effects of a faint young Sun, and who included some limiting cases of additional interior energy due to the phase separation of helium from liquid metallic hydrogen at megabar pressures (Stevenson & Lissauer 1977a). Fortney & Hubbard (2003) looked at the evolution of Saturn and tested a number of previously published phase diagrams for H/He phase separation. Saumon & Guillot (2004) investigated the sensitivity of Jupiter cooling models to various hydrogen EOSs, which can predict quite different temperatures in the deep interior of the planet. All of these models used the Burrows et al. (1997) atmosphere grid.

In Figures 7 and 8, we compare Jupiter and Saturn evolution models to those of Fortney & Hubbard (2003). The old and new models make the same assumptions regarding solar luminosity...

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**Table 2**

(Continued)

| Gravity | \(T_{\text{eff}}, 1.0\) | \(T_{10}, 1.0\) | \(T_{\text{eff}}, 0.7\) | \(T_{10}, 0.7\) | \(T_{\text{int}}\) |
|---------|-----------------|-----------------|-----------------|-----------------|-----------------|
| 11.2    | 177.2           | 628.6           | 176.6           | 625.7           | 175             |
|         | 135.8           | 445.4           | 134.4           | 440.0           | 131             |
|         | 112.3           | 347.5           | 110.0           | 339.2           | 104             |
|         | 99.5            | 296.9           | 96.1            | 286.5           | 87              |
|         | 94.0            | 275.9           | 90.3            | 264.2           | 78              |
|         | 89.2            | 257.0           | 84.1            | 242.3           | 69              |

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**Notes.** Surface gravities are in m s\(^{-2}\). A metallicity of \([M/\text{H}] = +1.0 (10\times\) solar) is assumed. "0.7" and "1.0" mean 0.7 and 1.0 times the current Saturnian incident flux.
Table 3

Uranus and Neptune Grids at Four Levels of Solar Flux

| Gravity | $T_{\text{eff}}, 0.12N$ | $T_{\text{eff}}, 1.0N$ | $T_{\text{eff}}, 1.0U$ | $T_{\text{eff}}, 1.8U$ |
|---------|------------------------|-----------------------|----------------------|----------------------|
| 4.0     | 32.66                  | 88.64                 | 49.11                | 48.71                |
|         | 37.37                  | 105.39                | 56.31                | 50.38                |
|         | 44.89                  | 134.43                | 68.06                | 54.11                |
|         | 55.11                  | 177.20                | 85.86                | 60.87                |
|         | 68.26                  | 231.89                | 111.00               | 71.96                |
|         | 86.23                  | 301.80                | 146.36               | 88.21                |
|         | 109.12                 | 396.53                | 196.11               | 109.93               |
|         | 137.31                 | 513.03                | 265.95               | 137.48               |
|         | 217.16                 | 1086.00               | 551.01               | 217.15               |
| 5.0     | 32.63                  | 85.80                 | 47.82                | 48.59                |
|         | 37.55                  | 101.83                | 54.82                | 50.28                |
|         | 44.85                  | 129.67                | 66.14                | 54.03                |
|         | 55.09                  | 170.80                | 83.13                | 60.81                |
|         | 68.46                  | 224.03                | 107.23               | 71.88                |
|         | 86.23                  | 291.63                | 141.08               | 88.18                |
|         | 109.12                 | 383.20                | 189.11               | 110.26               |
|         | 137.31                 | 512.66                | 256.60               | 137.66               |
|         | 217.05                 | 1048.68               | 531.44               | 217.13               |
| 6.3     | 32.60                  | 83.23                 | 46.61                | 48.47                |
|         | 37.32                  | 98.37                 | 53.36                | 50.21                |
|         | 44.85                  | 124.96                | 64.25                | 53.95                |
|         | 55.06                  | 164.66                | 80.49                | 60.75                |
|         | 68.20                  | 217.54                | 104.15               | 71.83                |
|         | 86.39                  | 282.31                | 136.28               | 88.47                |
|         | 109.12                 | 369.37                | 181.83               | 110.17               |
| 7.9     | 32.58                  | 80.44                 | 45.29                | 48.38                |
|         | 37.31                  | 95.08                 | 51.95                | 50.16                |
|         | 44.83                  | 120.47                | 62.44                | 53.89                |
|         | 55.06                  | 158.62                | 77.96                | 60.71                |
|         | 68.68                  | 209.94                | 100.58               | 71.77                |
|         | 86.38                  | 272.52                | 131.26               | 87.81                |
|         | 109.11                 | 356.83                | 175.23               | 109.92               |
| 10.0    | 32.54                  | 77.98                 | 44.08                | 43.11                |
|         | 37.28                  | 91.67                 | 50.46                | 50.05                |
|         | 44.82                  | 116.07                | 60.67                | 53.85                |
|         | 55.05                  | 152.70                | 75.50                | 60.60                |
|         | 68.66                  | 202.10                | 96.96                | 71.72                |
|         | 86.37                  | 262.93                | 126.39               | 88.03                |
|         | 109.12                 | 343.60                | 168.27               | 110.16               |
| 12.6    | 32.53                  | 75.61                 | 42.88                | 48.26                |
|         | 37.27                  | 88.63                 | 49.11                | 49.98                |
|         | 44.83                  | 111.89                | 58.97                | 53.78                |
|         | 55.03                  | 146.97                | 73.15                | 60.60                |
|         | 68.45                  | 193.69                | 93.14                | 71.70                |
|         | 86.23                  | 252.90                | 121.35               | 87.95                |
|         | 109.12                 | 331.47                | 161.88               | 110.09               |
| 13.0    | 32.53                  | 75.61                 | 42.88                | 48.26                |
|         | 37.27                  | 88.63                 | 49.11                | 49.98                |
|         | 44.83                  | 111.89                | 58.97                | 53.78                |
|         | 55.03                  | 146.97                | 73.15                | 60.60                |
|         | 68.45                  | 193.69                | 93.14                | 71.70                |
|         | 86.23                  | 252.90                | 121.35               | 87.95                |
|         | 109.12                 | 331.47                | 161.88               | 110.09               |

Notes. Surface gravities are in m s$^{-2}$. A metallicity of [M/H] = +1.5 (~30× solar) is assumed. "0.12N" and "1.0N" mean 0.12 and 1.0 times the current Neptunian incident flux, while "1.0U" and "1.8U" mean 1.0 and 1.8 times the current Uranian incident flux. The temperatures at 1 and 10 bars are provided.

and planetary structure, so the only differences are due to the model atmosphere grids. For both planets, a helium mass fraction (Y), relative to hydrogen, of 0.27 is used in the adiabatic H/He envelope. An rocky (zero-temperature ANEOS olivine) core mass of 10 $M_\oplus$ is used for Jupiter, and 21 $M_\oplus$ for Saturn. Within the H/He envelope, the zero-temperature ANEOS water EOS is used to mix in a mass fraction of 0.059 and 0.030 of “metals” in Jupiter and Saturn, respectively. In Fortney & Hubbard (2003) these choices reproduced the current radius and axial moment of inertia (obtained from more detailed structure models) at the time the planets cooled to their known $T_{\text{eff}}$ values. As in Fortney & Hubbard (2003) the heat content of the rock...
Figure 5. Uranus model atmosphere grid at 1.0 \( L_\odot \). Red is the lowest gravity, 4.0 m s\(^{-2}\), while yellow is the highest, 12.6 m s\(^{-2}\). The \( x \)- and \( y \)-axes are the same as in Figures 3 and 4, meaning the \( T_{\text{eff}} \)s are solid lines and \( T_{\text{int}} \)s are dotted lines.

(A color version of this figure is available in the online journal.)

Figure 6. Neptune model atmosphere grid at 1.0 \( L_\odot \). Red is the lowest gravity, 4.0 m s\(^{-2}\), while yellow is the highest, 12.6 m s\(^{-2}\). The grid is generally similar to that for Uranus, shown in Figure 5, but since the incident flux upon the planet is smaller, one generally find a smaller \( T_{\text{eff}} \) for a given \( T_{\text{int}} \). The \( T_{\text{eff}} \)s are solid lines and \( T_{\text{int}} \)s are dotted lines.

(A color version of this figure is available in the online journal.)

and water are neglected in the evolution calculation. Fortney & Hubbard (2003) use a Bond albedo 0.343 was assumed for both planets at all ages, while now we use the self-consistent grids. The cooling times are modestly prolonged, as will be discussed in detail in Section 3.3.

A particular interesting difference shown in Figure 8 is the larger radii for the new planet models at young ages, which is most pronounced in Saturn. This is a manifestation of the arbitrary initial condition (a hot, \( \sim 3 R_J \), adiabatic sphere) along with the slowed cooling in the 700–400 K \( T_{\text{int}} \) range compared to previous models (See Section 3.3). The initial conditions for cooling are tied to details of the energetics of planet formation and are not well understood (Marley et al. 2007a).

The revised cooling age for Saturn does little to change the long-standing problem that the planet is much more luminous than homogeneous models predict (Pollack et al. 1977). This has long been attributed to the phase separation (demixing) of helium from liquid metallic hydrogen. This helium solubility is thought to be minimized at pressures of several megabars, at pressures where the (gradual?) dissociation and ionization of hydrogen is nearly completed (Stevenson 1975). The phase diagram of H/He mixtures is beyond the realm of current experiment, but recent advances in first principles calculations of the H/He phase diagram (Lorenzen et al. 2009; Morales et al. 2009) should be tested in evolution models (Hubbard et al. 1999; Fortney & Hubbard 2003), to see if the additional energy source from this “helium rain” can explain Saturn’s luminosity. Previously calculated phase diagrams were tested in Fortney & Hubbard (2003) and were found to not explain Saturn’s thermal evolution. A complication that must be addressed in the future is whether the deep interior temperature gradient becomes...
dramatically super-adiabatic in the face of helium composition gradients (Stevenson & Salpeter 1977a; Fortney & Hubbard 2003).

The model calculations for Jupiter, which yield an age of 5.3 Gyr, rather than 4.6 Gyr, could have important implications for the planet. Jupiter’s atmosphere is clearly depleted in helium, according to Galileo Entry Probe data (von Zahn et al. 1998), which is a strong indication that helium phase separation has occurred in this planet. Furthermore the atmosphere’s depletion in neon (Mahaffy et al. 2000) is strongly suggestive of helium demixing as well, as neon is expected to preferentially dissolve into helium-rich droplets (Roulston & Stevenson 1995; Wilson & Militzer 2010). The inclusion of the additional energy release due to this demixing will further prolong Jupiter’s cooling (Hubbard et al. 1999), leading to a worse match with observations.

However, Saumon & Guillot (2004) have investigated cooling models of Jupiter with a variety of hydrogen EOSs, that predict a wide range of temperatures in Jupiter’s deep interior, which led to evolutionary ages for homogeneous models as short as 3 Gyr. If the deep interior temperatures in Jupiter are lower than those found with the Saumon et al. (1995) EOS used here, then it is possible that a combination of the model atmospheres presented here, helium rain (which prolongs the evolution), and colder interior temperatures (which quickens the evolution) could yield a good match to observations. Recent work on the hydrogen EOS, both theoretically (Nettelmann et al. 2008; Militzer et al. 2008), and experimentally (Holmes et al. 1995; Collins et al. 2001), do yield temperatures lower than predicted by Saumon et al. (1995), so this avenue is plausible.

3.2. Uranus and Neptune

The long-standing problem for Uranus and Neptune has been that both of these planets are colder at the present day than cooling models predict. This is a reverse of the situation for Saturn. This issue is discussed in some detail in Podolak et al. (1991) and Hubbard et al. (1995), and in the general literature in Hubbard & Macfarlane (1980). In order to understand how advances in input physics over the past 30 years in the EOSs affect the thermal evolution of these planets, we have computed a set of evolution models that use the physics of the Hubbard & Macfarlane (1980) models and compared them to our new calculations. The models presented in Hubbard & Macfarlane (1980) have three distinct, adiabatic, layers. The H/He envelope uses the EOS of Slattery & Hubbard (1976), the ‘icy’ layer uses a mixture the H2O, NH3, and CH4 EOS from Zharkov & Trubitsyn (1978), and the rocky core (a mixture of silicon, magnesium, iron, oxygen, and sulfur) is also from Zharkov & Trubitsyn (1978). Hubbard & Macfarlane (1980) also make estimates for the specific heat capacity of the icy and rocky layers. Our implementation of the Hubbard & Macfarlane (1980) models agree well with the original, particularly for Uranus, and yield slightly shorter cooling times for both planets (dashed curves in Figure 9), compared to their work.

To investigate how updated EOSs affect the evolution, we can create cooling models that use the same ice-to-rock ratio as used in Hubbard & Macfarlane (1980), 2.71-to-1, and the same Graboske et al. (1975) atmosphere grid. But instead we use updated EOSs for all three layers. These are the Saumon et al. (1995) EOS for H/He and the Sesame EOSs of “water 7154” and “dry sand” (Lyon & Johnson 1992) for water and rock, respectively. These tabulated ice and rock EOSs include calculations of the density- and temperature-dependent free energy at every temperature/density point, so no assumption must be made for the average heat capacity. In Figure 9, we compare cooling tracks with old and new EOSs. Following previous work, we plot these tracks backward in time from the current day, to see what initial values of Teff could explain the current planets. The updated EOS yields much faster evolution for both planets (dotted curves). The change for Neptune is enough to allow the planet have an initially “hot start.” However, Uranus models must start at a very low Teff to explain the planet’s current low Teff. Using these same new interior models, but
with our new model atmosphere grids, yield the thick solid curves in Figure 9. These lead to slower cooling for both planets, most dramatically for Uranus. Neptune’s evolution is still approximately consistent with an arbitrarily hot start at formation. This last finding agrees with the work published in Fortney & Nettelmann (2010).

While the three-layer models presented in Hubbard & Macfarlane (1980) were at the time consistent with observational constraints on their interior structure, that is no longer the case. Neither the Hubbard & Macfarlane (1980) models, nor our new implementation of their three-layer models (with the revised EOSs), are consistent with the gravity fields of these planets. To further expand our treatment of Uranus and Neptune, we calculated new structure models, using the methods described in Nettelmann et al. (2008) and Fortney & Nettelmann (2010). We then investigated the thermal evolution of these models that are also consistent with the constraints on current structure.8

As in Fortney & Nettelmann (2010), these models also use a three-layer structure, but include some water mixed into the H/He layer, and some H/He mixed into the water layer, above the rock core. The outer layer is predominantly H/He with a helium mass fraction, relative to hydrogen (Y), of 0.27 (the H-REOS and He-REOS EOSs; Nettelmann et al. 2008) with a 0.30 mass fraction of water (the EOS of French et al. 2009). The middle layer is mostly fluid water (mass fraction 0.878, beginning at 0.20 Mbar for Uranus, and 0.852, beginning at 0.10 Mbar for Neptune), with a small admixture of H/He. Both of these layers are adiabatic. The core is rock (Hubbard & Marley 1989) with a mass of 1.51 M⊕ for Uranus and 2.85 M⊕ for Neptune. For the evolution models, the rock core uses a radioactive luminosity from Guillot et al. (1995) and a specific heat capacity of 1 Jg−1K−1. The full allowed range of Uranus/Neptune interior compositions are explored in Fortney & Nettelmann (2010).

The fit to the Graboske et al. (1975) grids use T1 = 73 K (K = 1.418) and T1 = 78 K (K = 1.571) for Uranus and Neptune, respectively, including the gravity dependence.

Evolutionary calculations for these model planets are shown in Figure 10. We can reproduce well the current T_eff of Neptune (blue models) with our new model atmosphere grid (solid curves), as well as the older grid (dashed). The latter models agree well with work published in Fortney & Nettelmann (2010) which shows that the cooling times are insensitive to details of structure assumptions within the range allowed by the observational uncertainties. Therefore, there is a plausible consistency for the planet: the current interior structure and cooling history can be matched by one model. As shown in Figure 10, the mismatch for Uranus becomes appreciably larger with the new model atmospheres, in agreement with Figure 9. For Uranus in particular the model indicates a very slow change in T_eff with time in the current era, due to the larger incident flux and higher T_eq than for Neptune. Therefore small changes in the model atmosphere can lead to dramatic changes in cooling times, as seen in Figures 9 and 10. Another manifestation of Uranus’ slow cooling is shown by the thin red curve in Figure 9. This shows that a tiny change in the current T_int, to the maximum allowed by observation (1σ error bar; Pearl & Conrath 1991) can dramatically alter the calculation of the past cooling history.

8 These particular curves use T1 = 73 and 78 K for the current Uranus and Neptune, to better allow the static structure model to match the T_eff at the current time, at the expense of a slightly worse match to the observed T1. However, changes in T1 by a few degrees in either direction at the current time, which adjusts the interior structure, has little effect on the cooling history.

Figure 10. Thermal evolution of Uranus (red) and Neptune (blue) for models that match the current gravity field constraints. The thick solid curves use the model atmosphere grids presented in this work. The dashed curves are similar to those presented in Fortney & Nettelmann (2010), which used a fit to the Graboske et al. (1975) grid. When the T_eq of each planet reaches the observed values, the interior structure of each planet is consistent with the gravity field. At 4.56 Gyr, the radii of Uranus and Neptune are 25,730 km and 24,670 km, respectively. Inset: a zoom-in on the current era, which shows that the T_eq of Neptune is well reproduced, but the model Uranus is far too luminous. Measured T_eq and error bars are taken from Guillot (2005). (A color version of this figure is available in the online journal.)

3.3. Effects of the Atmosphere Grids

As shown in Figures 7–10, a general finding of our work is that the cooling of our solar system’s giant planets is slowed with the new model atmospheres. The main reason is higher atmospheric opacity, due to improvements in opacity databases, especially at high temperature, as well as the inclusion of opacity sources not previously known in 1975 or 1997. Here, we investigate the reasons for these differences in atmospheric structure and cooling. We will first examine Jupiter and Saturn.

It is important to note that the agreement between the Burrows et al. (1997) grid and our grids are best at current (low) T_int values. This is not necessarily surprising. Both works use the same model atmosphere code (that of Marley et al. 1996; Marley & McKay 1999). However, the opacity databases used have changed significantly over the past 14 years, most importantly at high T_int values. At low temperature, the only remaining opacity sources are methane vapor and H2 collision induced absorption (CIA). At warmer temperatures, observations of numerous T-type brown dwarfs have necessitated dramatic revisions to model atmospheres since 1997, including the inclusion of important new opacity sources, such as the alkali metals (Burrows et al. 2000; Allard et al. 2001). In addition, high-temperature molecular opacity databases, which were in their infancy in 1997, are now becoming more complete, which generally leads to higher opacities. Compared to Figure 2 of Burrows et al. (1997) we find much smaller detached radiative zones below the photosphere, over a narrower range of T_int. (In fact, for the Jupiter grid specifically, only the 450 K and 600 K models possess them.)

At constant T_int, a smaller or nonexistent detached radiative zone leads directly to a lower specific entropy adiabat, as shown in Figure 11 for models at 596 and 417 K, representing Jupiter at ages of 10 and 32 Myr, respectively. In black we show the standard 3× solar metallicity models. In orange we show the same calculation, but with 1× solar metallicity. The
Equation (4). For example, a comparison with Figure 12. We plot planet radius versus differences between the old and new atmosphere grids can be (A color version of this figure is available in the online journal.) extent with a shallower temperature gradient, again leading to a cooler adiabat. The removal of the alkali opacity leads to a detached radiative zone that is larger in opacity, a higher pressure photosphere, and lower specific entropy adiabat. The atoms removed. From black to orange, decreased metallicity leads to decreased orange curves are the same, but feature solar metallicity. The magenta curves × of the Jupiter model at 32 and 10 Myr and feature 3× solar metallicity. The magenta curves in Figure 7 shows that the new (black) models, compared to the red models, cool more quickly at Tint > 800 K, but more slowly below 800 K. Below 200 K, the differences are quite small. The same general picture is true for Saturn. (A color version of this figure is available in the online journal.)

Figure 11. Model pressure–temperature profiles of Jupiter at 417 K (g = 20.1 m s−2) and 596 K (g = 17.7 m s−2). Thick lines indicate convective energy transport, while thin lines indicate radiative energy transport. Cloud condensation curves are in dotted black. The equal-abundance curves of CH4/CO and NH3/N2 are dashed. The solid black curves represent the atmosphere of the Jupiter model at 32 and 10 Myr and feature 3× solar metallicity. The orange curves are the same, but feature solar metallicity. The magenta curves are also solar metallicity, but with the opacity of neutral atomic Na and K atoms removed. From black to orange, decreased metallicity leads to decreased opacity, a higher pressure photosphere, and lower specific entropy adiabat. We are still unable to match the large extent of the radiative zone that is larger in extent with a shallower temperature gradient, again leading to a cooler adiabat. (A color version of this figure is available in the online journal.)

Figure 12. Radii of models of Jupiter and Saturn from Figure 7 as a function of Tint. (1 Rj is 71,492 km, Jupiter’s equatorial radius.) Recall that radii, S, and T10 are all monotonic functions of each other. As the planets cool, their radii contract, and S and T10 decrease. The open circles are time steps at ages of 106, 107, 108, 109, and 1010 years. Steeper dR/dTint slopes lead to slower cooling (see the text). For instance, a comparison with Figure 7 of Tint for Jupiter shows that the new models, compared to the red models, cool more quickly at Tint > 800 K, but more slowly below 800 K. Below 200 K, the differences are quite small. The same general picture is true for Saturn.

Figure 13 shows that the new models lead to slower cooling from Tint of ∼800 K to the present Tint, although the differences are extremely small at Tint below 200 K.

In Figure 13 we show model P–T profiles for Jupiter’s atmosphere, corresponding to the new cooling curve for Jupiter in Figure 7. While the early evolution is highly uncertain (e.g., Marley et al. 2007a), we find that at 1 Myr Jupiter’s atmosphere had only one (deep) convective zone, while a second, detached convective zone appears for a few tens of millions of years, from perhaps ∼5–50 Myr. We also find that Jupiter’s water clouds formed at an age of ∼30 Myr, while the ammonia clouds began to condense at ∼1 Gyr.

Figure 14 shows that the Uranus and Neptune evolution models generally show an effect similar to that seen for Jupiter and Saturn. Here, the new grids always lead to a smaller Tint at a given radius. Hence, the cooling is always slower when using the grids, compared to those of Graboske et al. (1975). It is clear from Figure 14 that the apparently small difference between the grids at low Tint becomes magnified because the cooling is so slow. Even at higher Tint, farther back into the past, the differences between the two grids is larger than in Neptune. There, the good agreement at low Tint is an effect of the Graboske et al. (1975) grids being ad hoc “tuned” to agree well with the current Uranus and Neptune, with Pj the reference pressure being changed from 1 bar to 0.750 bar for Uranus and 0.861 bar for Neptune (see Hubbard & Macfarlane 1980). As one moves to higher Tint, there is no reason to expect this tuning of the grid to hold, so the old and new grids diverge.

We now turn to the effect on evolution. Given our discussion above, a given drop in S between two identical structure models will occur at a lower Tint for a fully convective atmosphere, which leads to a longer time step in Equation (4), since this step goes at Tint to the fourth power. Another way to look at cooling differences between the old and new atmosphere grids can be gleaned from Figure 12. We plot planet radius versus Tint, as the radius can serve a proxy both for interior specific entropy (parameterized by T10), and we can visually examine the surface gravity and Tint changes experienced in the model. On this plot regions where the new atmosphere grid lead to slower cooling are where the slope dR/dTint, our proxy for dS/dTint, is steeper for the black curves than that of the red curves. For a given change in Tint, they have a larger ΔS, meaning a longer time step from Equation (4). For example, a comparison with Tint versus time
these planets’ non-axial non-dipolar-dominated magnetic fields convection in these planets, and in particular the generation of complications arise in Uranus do not arise in Neptune, or to a constituent materials. It appears that whatever deep interior is based predominantly on modern updates to the EOSs of Model pressure–temperature profiles of Jupiter from log \( t = 6 \) to 9.5 years, in steps of 0.5. The thin black curves are radiative regions while thick black curves are convective regions. Cloud condensation curves are in dotted black. The equal-abundance curves of CH\(_4\)/CO and NH\(_3)/N\(_2\) are dashed. The rightmost profile is \( T_{\text{eff}} = 976 \) K, \( g = 11.4 \) m s\(^{-2}\) at 1 Myr. The profiles third and fourth from the right (596 K, 17.7 m s\(^{-2}\), 10 Myr, and 417 K, 20.1 m s\(^{-2}\), 32 Myr) have a detached convective zone. From the models, it appears that Jupiter’s water clouds formed at an age of \( \sim 30 \) Myr, while the ammonia clouds began to condense at \( \sim 1 \) Gyr.

(A color version of this figure is available in the online journal.)

4. DISCUSSION AND CONCLUSIONS

Our own giant planets serve as our calibrators for the evolutionary theory used to understand the thermal evolution of extrasolar giant planets (e.g., Hubbard et al. 2002; Guillot 2005; Fortney & Nettelmann 2010; Baraffe et al. 2010). As new EOSs come online, better understanding of interior energy transport develops, or new calculations of atmospheric structure or opacities are made, the problem of the cooling of the giant planets needs to be revisited. We have investigated “standard” cooling models for these planets, where the planetary luminosity is predominantly due to the slow release of remnant formation energy, within adiabatic layers beneath the radiative atmosphere.

At our calculations are taken at face value, we can robustly conclude, as have authors before us, that Saturn is quite overluminous, necessitating a large role for helium phase separation over the past 2 Gyr (Stevenson & Salpeter 1977a; Fortney & Hubbard 2003). For Jupiter, the model cooling age is now modestly too long, which may suggest that the interior temperatures are colder than yielded by our models, as has been hinted at previously. Although Hubbard et al. (1999) have shown that cooling ages for Jupiter of 3.5 Gyr are possible in the absence of incident solar flux (a Bond albedo of 1) for this H/He EOS, extreme atmospheric reflectivity does not seem to be a realistic pathway to faster cooling.

Like others, we find that Uranus is quite underluminous. Podolak et al. (1991) have suggested that a statically stable interior, unable to convect due to composition gradients, may be the best explanation. However, these same models for Neptune can match the planet’s \( T_{\text{eff}} \) at age of 4.5 Gyr. The improvement is based predominantly on modern updates to the EOSs of constituent materials. It appears that whatever deep interior complications arise in Uranus do not arise in Neptune, or to a much smaller degree. This could have profound implications for convection in these planets, and in particular the generation of these planets’ non-axial non-dipolar-dominated magnetic fields (see, e.g., Stanley & Glatzmaier 2009, for a review of dynamo modeling).

Using the interior statically stable geometry suggested by Podolak et al. (1991) and Hubbard et al. (1995), Stanley & Bloxham (2004, 2006) were able to reproduce the main features of the magnetic fields of Uranus and Neptune by hypothesizing dynamo action in only an outer shell in both planets. However, we find that such a picture may not be viable for Neptune. More recently Gómez-Pérez & Heimpel (2007) have constructed three-dimensional dynamo models with radial variable electrical conductivity, and found similar good agreement with observations without adhering to the statically stable interior geometry. More work in this area is certainly needed.

The summary figure of the models presented here—the luminosity of the giant planets with age—is shown in Figure 15. Of course the luminosities at young ages for all planets are uncertain, and depend strongly on the details of the formation process (Marley et al. 2007a). Lower post-formation luminosities are certainly realistic, although at gigayear ages the details are not important. In addition the cooling curve of Uranus should be regarded with suspicion.

One could certainly envision more complex models of the interiors of these planets, particularly for Uranus and Neptune. We have modeled the “fluid ice” component of these planets with a water EOS, but some previous authors have chosen instead to use mixtures of water, ammonia, and methane. Shock
experiments have studied a C-N-O-H mixture called “synthetic Uranus” for use in ice giant modeling (Nellis et al. 1997; Hubbard et al. 1991). The relative amounts of C, N, and O in these planets is not constrained by structure models or formation theory. Also, one must remember that the high-pressure EOS of planetary material are uncertain. Baraffe et al. (2008) have quantitatively explored the use of different EOSs for water, rock, and iron on the structure and evolution of Jupiter- and Neptune-class exoplanets. The evolution of Uranus and Neptune could be most affected by EOS uncertainties.

We also caution that the good agreement with observations for the Neptune cooling models could be a coincidence. Theory and experiment have probed the phase diagram of pure carbon and have shown that it is solid diamond at Neptune-interior P-T conditions. A rain of solid diamond has been suggested for the interiors of Uranus and Neptune (Ross 1981; Benedetti et al. 1999; Eggert et al. 2010), which could, at least in principle, be an additional energy source that preferentially powers Neptune more strongly than Uranus, to explain their dichotomy. These avenues should be explored in the future.

There are a few paths toward improving the atmosphere grids presented here. For Jupiter and Saturn, one could investigate the reduced He/H ratio as the planets age, which would affect the hydrogen CIA that is an important infrared opacity source in these atmospheres. We recommend updating CIA opacity in general, as the state-of-the-art in H-CIA opacity calculations (e.g., Borysow 2002) are now showing some mismatches in modeling brown dwarf spectra (Cushing et al. 2008). The inclusion of condensate clouds, either from equilibrium chemistry, such as ammonia and water, or a methane-derived photochemical haze, are important in accurately modeling the energy balance and temperature structure of these atmospheres. Whether this could be understood well enough to predict with confidence the effects of clouds over the range of past $T_{\text{eff}}$, atmospheric chemical mixing ratios, and surface gravity, in a one-dimensional planet-wide average model atmosphere, is an open question. It seems likely that further improvement toward understanding the cooling of the planets will likely come from work on the EOS of planetary materials.

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Figure 15. Luminosity of the giant planets as a function of age. Observed values (Pearl & Conrath 1991) are shown as black dots. The values for Uranus and Neptune nearly overlap. Estimates at young ages are highly uncertain, and depend strongly on the details of the formation process, especially for Uranus and Neptune. Note that Uranus and Neptune cross at age of 1 Gyr, and Neptune becomes cooler.
