Directed flow of transported and non-transported protons in Au+Au collisions from UrQMD model

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The directed flow of inclusive, transported and non-transported (including produced) protons, as well as antiprotons, has been studied in the framework of Ultra-Relativistic Quantum Molecular Dynamics approach (UrQMD model) for Au+Au collisions at \( \sqrt{s_{NN}} =7.7, 11.5, 19.6, 27, 39, 62.4 \) and 200 GeV. The rapidity, centrality and energy dependence of directed flow for various proton groups are presented. It is found that the integrated directed flow decreases monotonically as a function of collision energy for \( \sqrt{s_{NN}} =11.5 \) GeV and beyond. However, the sign-change of directed flow of inclusive protons, seen in experimental data as a function of centrality and collision energy, can be explained by the competing effect of directed flow between transported and non-transported protons. Similarly the difference in directed flow between protons and antiprotons can be explained.

Our study offers a conventional explanation on the cause of the \( v_1 \) sign-change other than the antiflow component of protons alone which is argued to be linked to a phase transition.

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I. INTRODUCTION

Relativistic Heavy Ion collisions, involving two nuclei moving close to the speed of light, produce thousands of particles. The collective motion of the outgoing particles is of special interest because it carries important information about the bulk properties of the system. A handle into the study of such collective motion makes use of the azimuthal distributions of detected particles in non-central collisions [1]. For a quantitative description, such distribution is conventionally decomposed [2] by a Fourier series

\[
E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left( 1 + \sum_{n=1}^{\infty} 2v_n \cos n\phi \right)
\]

where \( \phi \) denotes the angle between the particle’s azimuthal angle in momentum space and the reaction plane angle. The reaction plane is defined by the collision axis and the line connecting the centers of two nuclei. The various coefficients in this expansion can be calculated as [2]:

\[
v_n = \langle \cos n\phi \rangle
\]

The first and the second coefficients are referred to as directed (\( v_1 \)) and elliptic flow (\( v_2 \)), respectively, and they both play important roles in describing the collective expansion in azimuthal space. Elliptic flow is produced by the conversion of the initial coordinate-space anisotropy into the momentum-space anisotropy, due to the developed large in-plane pressure gradient [3]. Directed flow, which is the focus of this study, describes the “side splash” of particles measured off mid-rapidity [3]. It probes the dynamics of the system in the longitudinal direction. The shape and magnitude of directed flow in the vicinity of midrapidity are of special interest, specially for protons, because they are sensitive to the equation of state (EOS) and may carry phase transition signal [7].

Directed flow has been measured at the AGS [10, 11], at the CERN SPS [12], and at RHIC [13-15]. In particular, the directed flow of protons at RHIC has been studied in detail by the STAR Collaboration, for Au+Au collisions at \( \sqrt{s_{NN}} =200 \) GeV [14] and at lower energies [14]. It is worthy of notice, that at energies studied by STAR, protons and antiprotons exhibit different \( v_1(y) \) slope in close-to-central collisions (5-30% at 200 GeV and 10-40% at low energies), and at low energies the proton \( v_1(y) \) slope changes its sign from negative as in peripheral collisions to positive as in close-to-central collisions. The sign-change of \( v_1(y) \) slope has been proposed as a possible signal of phase transition, it is thus necessary to identify other causes that may give rise to the similar sign-change of directed flow in the vicinity of \( y=0 \). Indeed it is mentioned in [17] that the observed \( v_1 \) for protons is a convolution of the directed flow of produced protons with that of protons transported from beam rapidity. Since transported protons come from the original projectile and target nuclei, they preserve the directed flow of spectators. Produced protons, on the other hand, tend to flow with the bulk. The flow direction of spectators and bulk are not necessarily equal; the final \( v_1 \) observed would then be the result of a competition between the two different proton sources.

In this work we study the interplay between the directed flow of transported protons and that of non-
transported protons, within the framework of the Ultra-relativistic Quantum Molecular Dynamics model (UrQMD) [19]. Note that although $v_1(y)$ calculated with UrQMD does not reproduce the measurement from Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV, as already pointed out in [17], the study of the contributions from transported and non-transported protons to the overall proton $v_1$ can offer insights into the competing dynamics which lead to the final observation of the sign of $v_1(y)$ and its slope in the vicinity of midrapidity.

II. TRANSPORTED AND NON-TRANSPORTED PARTICLES IN THE URQMD MODEL

UrQMD is a microscopic transport model based on the covariant propagation of all hadrons along classical trajectories in combination with stochastic binary scatterings, color string formation and resonance decay. This microscopic transport model describes the phenomenology of hadronic interactions at low and intermediate energies ($\sqrt{s} < 5$ GeV) in terms of interactions between known hadrons and their resonances. At higher energies($\sqrt{s} > 5$ GeV), the excitation of color strings and their subsequent fragmentation into hadrons dominates the multiple production of particles in the UrQMD model [19].

Fig. 1 schematically sketches the exitation and subsequent fragmentation ($\sqrt{s} > 5$ GeV) of a baryon-string [19]. In the first case, shown on top of the figure, the exitation energy is too low to produce new quark pair(s), and there is only one baryon A in the final state. In the second case, one diquark-antidiquark pair and one quark-antiquark pair are created. One of the initial quarks (white circle) combines with a newly produced diquark (black circles) to form the baryon B, the newly produced anti-diquark (brown circles) combines with a newly produced anti-quark to form the antibaryon C, and the newly produced quark together with the initial diquark form another baryon D. The third case is similar to the second one, and it shows the produced baryons and a meson. At the end baryon A has three initial quarks (3 iq, where iq stands for “initial quark”), baryon D and H each have two initial quarks (2 iq), baryon B has one initial quark (1 iq), and baryon G has zero initial quark (0 iq). The two anti-baryons (C and G) each have zero initial quark (0, iq). The more initial quarks can be found in a particle, the more initial information that particle carries. By tracing the number of initial quarks in a particle, we classify particles as produced or transported particles. In this article, baryons with three initial quarks are regarded as transported baryons, and all other baryons that have at least one produced quark are regarded as non-transported. A particular subgroup of the latter are the produced baryons with zero initial quarks. Produced baryons should be similar to anti-baryons in many respects as both groups are made of produced quarks.

After the process of fragmentation excitation of baryon-strings, baryons produced (mostly unstable baryons) are subject to multiple scatterings. When the energy of a binary collision is lower than 5 GeV ($\sqrt{s} < 5$ GeV), there will be no strings involved and there are no new quark pairs produced. During this process the unstable baryons do decay but the number of constituent quarks does not change. For example, in the case of a $\Lambda$ decay into a proton and a pion, one can still identify how many quarks in the daughter proton are originated from initial quarks by tracing the quark constituent of its parent, $\Lambda$.

III. ANALYSIS AND RESULTS

Fig. 2 shows the rapidity distribution of protons and anti-protons for Au+Au collisions at $\sqrt{s_{NN}} = 11.5$ GeV and 200 GeV, calculated with the UrQMD model. The selection on centrality (10%-70%) and transverse momentum $p_T$ ($0.4-1$ GeV/$c$) are chosen to match those used in [17]. The distribution of transported, non-transported, and produced protons are drawn separately. As expected, the transported protons peak at beam rapidity and the produced ones, at midrapidity. Not surprisingly, the distribution of produced protons is similar to that of anti-protons (to first order), and the remaining difference comes from their separate production mechanisms. For example, for each produced baryon there is an accompanying anti-baryon produced but that statement is not necessarily true for anti-baryons. In addition, antiprotons are subject to annihilation while protons are not. The transported (produced) protons accounts for...
To illustrate the effect of the mixture of initial and produced quarks on the shape of $v_1(y)$ Figure 3 shows $v_1(y)$ plotted for all proton (antiproton) groups for Au+Au collisions at $\sqrt{s_{NN}} = 11.5$ (left) and 200 (right) GeV, calculated with the UrQMD model.

FIG. 3: Rapidity dependence of $v_1$ for protons and anti-protons in Au+Au collisions at $\sqrt{s_{NN}} = 11.5$ GeV for centrality 10%-70%, from UrQMD calculation. See text for explanation on individual protons groups.

FIG. 4: The $v_1$ slope as a function of centrality for protons and anti-protons for Au + Au collisions at $\sqrt{s_{NN}} = 5$ (left) and 200 (right) GeV, calculated with the UrQMD model.

12% (2.1%) of inclusive protons at 11.5 GeV, and 0.91% (50%) at 200 GeV. The baryon stopping effect is seen at both energies. At midrapidity, transported protons dominate over produced protons at 11.5 GeV, while at 200 GeV, the opposite is true. Note that the sum of the yield of transported and produced protons does not give the inclusive proton yield because some of the protons can be regarded neither as transported nor produced. Those are protons that have 2 or 1 initial quarks, and they account for a large fraction of the total number of protons. By definition the inclusive proton yield is a sum of transported and non-transported proton yields.

To illustrate the effect of the mixture of initial and produced quarks on the shape of $v_1(y)$ Figure 3 shows $v_1(y)$
As the centrality decreases, the sign of the $v_1(y')$ slope gradually changes from positive to negative. This effect is more pronounced at higher collision energies, as seen in the inset of Fig. 5, and becomes negative at 62.4 GeV. The sign change of $v_1(y')$ is also observed in experimental data [18], although the energy at which the sign change occurs is lower (11.5 GeV). These findings suggest that the apparent “collapse” of $v_1$, defined by a flat shape of the proton $v_1(y')$, or the sign-change of the proton $v_1(y')$ slope, can be explained by the interplay between transported protons and non-transported protons.

IV. SUMMARY

Directed flow of inclusive, transported protons and non-transported protons (including produced protons), as well as anti-protons, has been studied with the UrQMD model at RHIC energies. It is found that the integrated directed flow decreases monotonically as a function of collision energy for $\sqrt{s_{NN}} = 11.5$ GeV and beyond. However, the sign-change of directed flow of inclusive protons, as a function of centrality and collision energy, can be explained by the competing effect of directed flow between transported and non-transported protons. Similarly, the difference in directed flow between protons and antiprotons can be explained. Our study identifies alternative causes of the $v_1$ sign-change other than the anti-flow component of protons alone which is argued to be linked to a phase transition.

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