Measurement of the mechanical loss of a cooled reflective coating for gravitational wave detection

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We have measured the mechanical loss of a dielectric multilayer reflective coating (ion-beam sputtered SiO$_2$ and Ta$_2$O$_5$) in cooled mirrors. The loss was nearly independent of the temperature (4 K $\sim$ 300 K), frequency, optical loss, and stress caused by the coating, and the details of the manufacturing processes. The loss angle was $(4 \sim 6) \times 10^{-4}$. The temperature independence of this loss implies that the amplitude of the coating thermal noise, which is a severe limit in any precise measurement, is proportional to the square root of the temperature. Sapphire mirrors at 20 K satisfy the requirement concerning the thermal noise of even future interferometric gravitational wave detector projects on the ground, for example, LCGT.

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I. INTRODUCTION

The development and observation of several interferometric gravitational wave detectors (LIGO 1, VIRGO 2, GEO 3, TAMA 4) on the ground are presently in progress. The sensitivity in the observation band of these detectors is expected to be limited by the thermal noise of the internal modes of the mirrors (this thermal noise is also a serious problem in laser frequency stabilization using a rigid cavity 5). Since the thermal noise of mirrors with less mechanical loss is smaller, research was done in an effort to reduce the loss in the mirrors. In order to decrease the thermal noise more effectively, it was proposed to cool the mirrors 6. In the Japanese future LCGT project 7, the mirrors will be cooled. In Europe, another future cryogenic interferometer project is being considered 8.

For estimating the temperature dependence of the thermal noise to evaluate the adequate mirror temperature for future cryogenic projects, measuring the loss in the low-temperature region is necessary. The loss of cooled sapphire (above 4 K), which is the mirror substrate of LCGT, has already been measured 9. Recent theoretical 10, 11, 12, 13, 14 and experimental 15, 16, 17 work has revealed that the loss of the reflective coating on the mirror surface has a large contribution to the thermal noise. The loss of a cooled coating is also an interesting issue in solid state physics (for example, Ref. 18). Nevertheless, a low-temperature measurement of the mechanical loss in the mirror reflective coating for gravitational wave detection had never been reported before ours.

We measured the mechanical loss of a cooled coating. The measured loss was almost constant between 4 K and 300 K. Thus, the amplitude of the coating thermal noise is proportional to the square root of the temperature. At 20 K, the summation of the thermal noise of the coating and sapphire substrate loss is sufficiently smaller than the goal sensitivity of LCGT. Our measurement provides some clues about the properties of the coating material at low temperature.

II. EXPERIMENTAL METHOD

A. Outline

In order to evaluate the mechanical loss of the coating, we prepared sapphire disks with and without a coating. After measuring the decay time of the excited resonant
TABLE I: Specifications of sapphire disks.

| Sample | disk thickness | heat process | coating vender |
|--------|----------------|--------------|----------------|
| Sample 1 | 0.5 mm         | not annealed | NAOJ            |
| Sample 2 | 1 mm           | not annealed | NAOJ            |
| Sample 3 | 1 mm           | not annealed | JAE             |
| Sample 4 | 1 mm           | annealed     | JAE             |
| Sample 5 | 0.5 mm         | not annealed | not coated      |
| Sample 6 | 1 mm           | not annealed | not coated      |

motions of these disks (ring down method) at low temperature, and calculating each Q-value, we obtained the loss of the coating by comparing these Q-values. In this experiment, it was possible to accurately estimate the cooled coating loss because the loss of the sapphire was extremely small at low temperature, and a coating was made on the thin disks in order to enhance the effect of the coating loss.

B. Samples

The sapphire disks were supplied by SHINKOSHA [19], Japan. The diameter of these disks was 100 mm. In order to observe the disk thickness dependence of the loss, two kinds of the disks, 0.5 and 1 mm thick disks, were prepared. The c-axis was perpendicular to the flat surface. Both sides were commercially polished (not super polished). The root mean square of the micro-roughness of the surfaces was about 0.1 nm. The coatings were made on some sapphire disks. The other uncoated disks were used to measure the Q-values without the coating. The specifications of the coating on the sapphire disks were almost the same as those of typical mirrors of the gravitational wave detectors, as follows. These disks were coated by means of ion-beam sputtering. This dielectric multilayer reflective coating consisted of 31 alternating layers of SiO$_2$ and Ta$_2$O$_5$. The total thickness was 4.8 $\mu$m. The optical thickness of a layer was a quarter of the wavelength, which was 1.064 $\mu$m. The resulting power reflectance was estimated to be 99.99%. For investigating the effect of the details in the manufacturing process, the coating was made by two venders: the National Astronomical Observatory of Japan (NAOJ) and Japan Aviation Electronics Industry, Ltd. (JAE). The latter made the coating on the mirrors of TAMA [4]. The JAE coating [20] was superior regarding low optical loss compared to that of NAOJ. Although the mirrors are usually annealed after the coating, only a disk with the JAE coating was annealed in this experiment. The specifications of the disks are summarized in Table I. We measured the Q-values of the first and third modes. The resonant frequencies are given in Table II. These frequencies with the coating were the same as those without the coating. The shapes of the first and third modes are shown in (a) and (b) of Fig. 1 respectively.

C. Measurement apparatus

Figure 2 is a schematic side view of the measurement apparatus. We adopted a nodal support system [21] to grasp the sapphire disk. In this system, only the center of the disk was fixed (the diameter of the contact area between the sapphire disk and the support was 2 mm). Since the center is the nodal point in almost all resonant modes, the contamination of the loss of the support system, itself, was small. All parts of this support were made of copper, which has a high thermal conductivity at cryogenic temperatures. We used an electrostatic actuator to excite the resonant vibration. The ring down of this resonant motion was monitored by an electrostatic transducer [22]. The bias voltage of the actuator and the transducer was a few hundreds volts. The loss caused by this transducer was negligible because the measured Q-values were independent of the bias voltage.

The top of the nodal support system was connected by stainless-steel rods to a vacuum tank. This chamber was immersed into liquid helium or nitrogen. The pres-
FIG. 2: Schematic side view of the measurement apparatus. Only the center of the sapphire disk was grasped by the nodal support system [21]. This support was made of copper. We used an electrostatic actuator to excite the resonant vibration. The ring down of this resonant motion was monitored by an electrostatic transducer. The top of the nodal support system was connected by stainless-steel rods to a vacuum tank. This chamber was immersed into liquid helium or nitrogen. The pressure in the cooled chamber was between $10^{-5}$ Pa and $10^{-3}$ Pa in most cases. A film heater was put on the top of the nodal support system to control the temperature between 4 K and 30 K. The two thermometers were fixed at the top and the bottom of the nodal support system.

sure in the cooled chamber was between $10^{-5}$ Pa and $10^{-3}$ Pa in most cases. In this pressure region, the gas damping was sufficiently small because the measured Q-values with the coating did not depend on the pressure. A film heater was put on the top of the nodal support system to control the temperature between 4 K and 30 K. The two thermometers were fixed at the top and the bottom of the nodal support system instead of the sapphire disk because the thermometer possibly increases the mechanical loss. Although, in principle, the temperature of the sapphire disk was the same as that of these thermometers, we confirmed this temperature homogeneity using a dummy sapphire disk with the thermometer. This dummy disk has never been adopted to measure the Q-values.

In order to check the ability of our measurement system, the typical differences between the measured Q-values with (close marks in Fig. 3) and without (open marks in Fig. 3) the coating are introduced. The thicknesses of the disks in graphs (a) and (b) were 0.5 mm and 1 mm, respectively. The coatings in graphs (a) and (b) were NAOJ (Sample 1) and annealed JAE (Sample 4). The disk without the coating in the graphs (a) and (b) was Sample 5 and Sample 6. The circles (blue in online) and squares (green in online) are the Q-values of the first and third modes. The solid and dashed lines represent the Q-values limited by the thermoelastic damping of the first and third modes, respectively [24].

In the low-temperature region, there was a large discrepancy between the Q-values with and without the coating [23]. An accurate evaluation of the cooled coating loss was possible. At room temperature, the differences between the Q-values with and without the coating were small (the marks with the coating in Fig. 3 completely overlap those without the coating except for the third mode of the 1 mm thickness disk). The evaluated coating loss angles at 300 K were not precise. The reason why the differences were small was that the thermoelastic damping in the sapphire disks was large at 300 K. The solid and dashed lines in Fig. 3 represent the Q-values limited by the thermoelastic damping of the first
TABLE III: Thicknesses and Young’s moduli of the disks and coating.

|                   | thickness | Young’s modulus  |
|-------------------|-----------|------------------|
| sapphire disk     | 1 mm or 0.5 mm | $4.0 \times 10^{11}$ Pa |
| coating           | 4.8 µm    | $1.1 \times 10^{12}$ Pa |

and third modes, respectively \[25\].

III. RESULTS

The formula \[11, 26, 27, 28\] of the loss angle, $\phi_{\text{coating}}$, which is the magnitude of the loss in the coating, derived from the measured Q-values is described as \[24, 30\]

$$
\phi_{\text{coating}} = \frac{1}{3} \frac{d_{\text{disk}}}{d_{\text{coating}}} \frac{Y_{\text{disk}}}{Y_{\text{coating}}} \left( \frac{1}{Q_{\text{with}}} - \frac{1}{Q_{\text{without}}} \right). \tag{1}
$$

The values, $Q_{\text{with}}$ and $Q_{\text{without}}$, are the measured Q-values with and without the coating. The parameters ($d_{\text{disk}}$, $d_{\text{coating}}$, $Y_{\text{disk}}$ and $Y_{\text{coating}}$) are the thicknesses and Young’s moduli of the sapphire disk and the coating, respectively. These values are summarized in Table III. The Young’s modulus of the coating is the average of those of SiO$_2$ (7.2 $\times$ 10$^{10}$ Pa \[31\]) and Ta$_2$O$_5$ (1.4 $\times$ 10$^{11}$ Pa \[31, 32, 33\]) \[11, 26, 27\], \[31\].

The coating loss angles derived from the measured Q-values are shown in Fig. 4 \[31\]. The circles (blue in online) and squares (green in online) represent the coating loss angles evaluated from the Q-values of the first and third modes, respectively. The four samples had similar loss angles. The disorder did not strongly depend on the temperature and resonant frequency. These loss angles were (4 $\sim$ 6) $\times$ 10$^{-4}$. (Some loss angles at 300 K had the large error bars. The upper limits of these error bars were the order of 10$^{-4}$.)

IV. DISCUSSION

A. Properties of the coating mechanical loss

Figure 4 implies that the coating loss is almost independent of the temperature between 4 K and 300 K. At room temperature, the coating loss is dominated by that of Ta$_2$O$_5$ \[27\]. Thus, it is expected that the loss of Ta$_2$O$_5$ is also the main component of the coating loss, and is constant in the low-temperature region. The loss of the SiO$_2$ does not change very much, either. Research showed that the loss of the fused silica film deposited by the electron beam evaporation was independent of the temperature \[37\]. The temperature dependence of these two kinds of thin SiO$_2$ is different from that of bulk silica. Many studies (for example, Refs. \[35, 38\]) found that the Q-value of the bulk SiO$_2$ has a local minimum (about 10$^{13}$) of around 30 K.

Recently, the thermoelastic damping of the coating at room temperature was investigated theoretically \[39, 40\]. Since the thermoelastic damping strongly depends on temperature in general, our result suggests that the contribution of thermoelastic damping is not a large part in the loss of the coating.

The measured cold coating loss angles were not affected by a change in the frequency between 0.52 kHz and 2.5 kHz. This result suggests that the loss which depends on the frequency (for example, the thermoelastic damping) does not dominate the coating loss around this frequency region.

The coating applies a stress on the substrate of the mirror. If the strain caused by this stress causes a loss, the coating loss on the thin disk in our experiment is different from that on thick mirrors. Fortunately, this scenario is rejected because the measured coating loss on a 0.5 mm thick disk was the same as that on a 1 mm thick disk.

It was reported that annealing improves the Q-values of fused silica \[11, 12, 13\]. There was no such effect on the coating in our samples. This result implies that the stress does not greatly change the loss because the annealing relaxes the stress produced during the coating process.

The loss of the NAOJ coating was about the same as that of the JAE coating. Since the optical loss of the NAOJ coating was larger than that of the JAE coating, the source of the optical loss does not have a large contribution on the mechanical loss.

In Fig. 5, a summary of our results with those of the measurements by other groups (SiO$_2$/Ta$_2$O$_5$) is listed (their references are written in the figure caption). The experiments of the other groups were at room temperature. The losses at 300 K in the coatings prepared by the various companies were on the order of 10$^{-4}$. The losses of the coating made by two laboratories, NAOJ and JAE, were almost the same in the low-temperature region. Thus, it is expected that the details of the coating manufacturing processes do not greatly affect the coating loss between 4 K and 300 K. This conclusion is in contrast with that of bulk fused silica: in Ref. \[43\], the best Q-value of the room temperature silica is about fifty-times larger than the worst one.

B. Coating thermal noise in interferometric gravitational wave detector

Our experiment shows that the coating loss is almost independent of the temperature between 4 K and 300 K. This result and the formulae in Refs. \[11, 13\] imply that the amplitude of the thermal noise caused by the coating loss is proportional to the square root of the temperature. The thermal noises at 20 K and 4 K are four and ten-times less than that at 300 K, respectively. Since the loss of sapphire decreases at low temperature, cooling reduces the thermal noise of the coating more modestly than that of the sapphire substrate loss. However, the
other methods used to suppress the coating thermal noise (reduction of the loss, other coating material, large scale laser beam, some ideas about coating thickness) are not more effective than the cooling, as follows.

In spite of investigations concerning a reduction of the coating mechanical loss, a method used to drastically suppress the loss was not found as shown in Fig. 5. Even if TiO$_2$ is doped [48], the thermal noise becomes about two-times smaller, because it is proportional to the square root of the loss angle [11, 13]. In our measurement, annealing was not useful.

Studies about other coating materials are also in progress (for example, Nb$_2$O$_5$/SiO$_2$, Ta$_2$O$_5$/Al$_2$O$_3$, Al$_2$O$_3$/SiO$_2$ [49, 50]). An obviously better material than SiO$_2$/Ta$_2$O$_5$ was not found.

Adopting a larger beam is one of the methods because the coating thermal noise is inversely proportional to the beam radius [11, 13]. When the beam becomes larger, the mirror must also be greater, owing to the diffraction loss. Because of technological limits about the scale of the mirror, the maximum beam radius is about 6 cm. Since the typical beam radius of the current km-class interferometers is about 3 cm, the reduction factor of the thermal noise is about two. Recently, a new beam profile, a flat-topped beam [51], was proposed to increase the beam scale without a large diffraction loss. The radius of this beam is 9 cm [51]. The thermal noise becomes three-times smaller [52].

In Ref. [53], it is considered to decrease the number of the coating layers effectively (from about thirty layers to a few layers) by putting another mirror behind the end mirror. The reduction factor of this idea is about four, at most, because the thermal noise is proportional to the square root of the thickness of the coating [11, 13]. The thermal noise of the non-periodic coating (the optical thicknesses of the layers are different from that of each other) is 1.4-times less than that of the usual coating (the optical thicknesses of the layers are the same) [54].

C. Adequate mirror temperature for future gravitational wave detector projects

The temperature dependence of the thermal noise of the mirrors was estimated in order to evaluate an adequate mirror temperature for future interferometric gravitational wave detector projects. The thermal noise of the mirrors is dominated by the contributions of the coating...
and the substrate losses [14]. The formula of the thermal noise of the coating derived in Ref. [13] was used. It was supposed that the coating loss angle is independent of the frequency and $4 \times 10^{-4}$. The substrate loss is the sum of the structure [55] and thermoelastic damping [56, 57]. It was assumed that the substrate Q-values are $10^5$ [45, 58, 59]. The length of the interferometer baselines and the beam radius at the mirrors were 3 km and 3 cm, respectively. These were typical values.

The evaluated results are given in Fig. 6. The solid thick lines represent the thermal noises of the sapphire mirrors at 300 K, 30 K, 20 K, and 4 K. The dashed line is the thermal noise of mirrors made from fused silica, which is the material of the current interferometers [1, 2, 3, 4], at 300 K as a reference. The thin line shows the goal sensitivity of the LCGT project [7] (the other future project, advanced LIGO [60], has a similar goal sensitivity).

D. Thermal noise in laser frequency stabilization

The thermal noise of the coating will be a serious problem in the frequency stabilization of the laser. Recent research [61] proved that the world-highest level of laser frequency stabilization using a rigid cavity is only three-times larger than the coating thermal noise. In the near future, the laser stabilization technique will achieve a fundamental physical limit, the coating thermal noise. According to our experiment, the coating thermal noise of the cavity at 4 K is ten-times smaller than that at room temperature. A cryogenic rigid cavity is one of the promising techniques to drastically improve the frequency stabilization.
V. CONCLUSION

In order to effectively suppress the thermal noise of interferometric gravitational wave detectors, it was proposed to cool the mirrors. To evaluate the thermal noise of the cryogenic mirrors, the mechanical loss in the cooled mirrors must be investigated. However, there had been no report about the loss of the reflective coating (SiO\textsubscript{2}/TaO\textsubscript{5}) at low temperature until our experiment. The coating loss measurement is also an interesting topic in material science.

Our measured loss angles, \((4 \sim 6) \times 10^{-4}\), were almost constant between 4 K and 300 K. Since the room-temperature coating loss is dominated by the loss of TaO\textsubscript{5}, it is expected that the loss of TaO\textsubscript{2} is also the main component in the low-temperature region. The loss in the ion-beam sputtered thin TaO\textsubscript{2} (and also SiO\textsubscript{2}) layer is independent of the temperature. The measured coating mechanical loss was not affected by changes of the frequency, optical loss, or stress caused by the coating and vendors.

Since the coating loss does not strongly depend on the temperature, the amplitude of the thermal noise of the coating is proportional to the square root of the temperature. As far as we know, there is no more effective method to suppress the coating thermal noise than cooling. The limit of laser frequency stabilization using a rigid cavity due to the coating thermal noise decreases by an order of magnitude when the rigid cavity is cooled from 300 K to 4 K. The amplitude of the total amount of the coating and substrate thermal noises of the sapphire mirrors at 20 K is sufficiently lower than the sensitivity of even future interferometric gravitational wave detector projects, for example, LCGT.

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