The speed–accuracy trade-off (SAT) is ubiquitous in decision tasks. While the neural mechanisms underlying decisions are generally well characterized, the application of decision-theoretic methods to the SAT has been difficult to reconcile with experimental data suggesting that decision thresholds are inflexible. Using a network model of a cortical decision circuit, we demonstrate the SAT in a manner consistent with neural and behavioral data and with mathematical models that optimize speed and accuracy with respect to one another. In simulations of a reaction time task, we modulate the gain of the network with a signal encoding the urgency to respond. As the urgency signal builds up, the network progresses through a series of processing stages supporting noise filtering, integration of evidence, amplification of integrated evidence, and choice selection. Analysis of the network’s dynamics formally characterizes this progression. Slower buildup of urgency increases accuracy by slowing down the progression. Faster buildup has the opposite effect. Because the network always progresses through the same stages, decision-selective firing rates are stereotyped at decision time.

Keywords: decision making, speed–accuracy trade-off, gain modulation, urgency, neural model, recurrent network

1 INTRODUCTION

Subjects in decision making experiments trade speed and accuracy at will (van Veen et al., 2008). Under otherwise identical conditions, they make faster, less accurate decisions when motivated to favor speed, and make slower, more accurate decisions when motivated to favor accuracy. The speed–accuracy trade-off (SAT) is ubiquitous across decision making paradigms, but while the neural mechanisms underlying decisions are generally well characterized (Gold and Shadlen, 2001; Schall, 2001), the neural basis of the SAT is an open question (Gold and Shadlen, 2002).

Experimental and theoretical work indicates that decisions result from mutual inhibition between neural populations selective for each option of a decision (see Gold and Shadlen, 2007), where intrinsic (recurrent) synapses support the integration of evidence over time (Usher and McClelland, 2001; Wang, 2002). Mutual inhibition ensures that the representation of evidence accumulating in each population comes at the expense of evidence accumulating in the other(s), implementing a subtractive operation (see Smith and Ratcliff, 2004; Bogacz, 2007). This neural framework instantiates a class of algorithms frequently referred to as the drift diffusion model (DDM), known to yield the fastest decisions for a given level of accuracy and the most accurate decisions for a given decision time (see Bogacz et al., 2006). Speed and accuracy can be traded in the DDM by adjusting the level of evidence required for a decision (the decision threshold; Gold and Shadlen, 2002). Empirical studies, however, indicate that decision-correlated neural activity reaches a fixed threshold at decision time (Hanes and Schall, 1996; Roitman and Shadlen, 2002; Churchland et al., 2008). How, then, can the SAT be accomplished by neural populations with a fixed decision threshold?

A convergence of evidence offers an answer. In neuronal networks with extensive intrinsic connectivity, integration times are determined by network dynamics (Usher and McClelland, 2001; Wang, 2002, 2008; Wong and Wang, 2006). Control of these dynamics is therefore a potential means of trading speed and accuracy. Gain modulation offers a means of control, where the magnitude of the neural response to sensory evidence changes as a function of a second input signal (Salinas and Thier, 2000; Salinas and Sejnowski, 2001). We propose that the neural encoding of elapsed time (Leon and Shadlen, 2003; Janssen and Shadlen, 2005; Genovesio et al., 2006; Mita et al., 2009) provides this second input.

We model a decision circuit in the lateral intraparietal area (LIP) of posterior parietal cortex with a recurrent network model. We choose LIP because this area is extensively correlated with decision making (Roitman and Shadlen, 2002; Huk and Shadlen, 2005; Thomas and Pare, 2007; Churchland et al., 2008), gain modulation (Andersen and Mountcastle, 1983; Andersen et al., 1985), and the encoding of temporal intervals (Leon and Shadlen, 2003; Janssen and Shadlen, 2005). In simulations of a decision task, the responsiveness of the network is modulated by an increasing function of time, referred to as the buildup of urgency (Churchland et al., 2008; Cisek et al., 2009). Across all task conditions, network activation reaches a fixed threshold at decision time, consistent with neural data (Roitman and Shadlen, 2002; Huk and Shadlen, 2005; Churchland et al., 2008). Our results are explained by network dynamics. As urgency builds up, the network progresses through a series of processing stages supporting noise filtering, integration of evidence, amplification of integrated evidence, and choice selection. The rate of urgency buildup controls the rate of this progression and consequently the SAT.
2 MATERIALS AND METHODS

A cortical decision circuit was simulated with a network from a class of models widely used in population and firing rate simulations of cortical circuits (Wilson and Cowan, 1973; Pouget et al., 2000; Douglas and Martin, 2007), including feature maps in V1 (Ben-Yishai et al., 1995), posterior parietal cortex (Salinas and Abbott, 1996; Standage et al., 2005), frontoparietal cortex (Cisek, 2006), and dorsolateral prefrontal cortex (Camperi and Wang, 1998). The model assumes a columnar organization, where intercolumnar interactions are characterized by a smooth transition from net excitation between adjacent columns to net inhibition between distal columns, furnishing a continuum of overlapping on-center, off-surround population codes (see Figure 1).

The model is constrained by signature characteristics of neural and behavioral data from visuospatial decision making experiments. The neural data we consider were recorded in LIP, but similar activity is seen in other decision-correlated cortical areas, e.g., the frontal eye fields (see Schall, 2002). These characteristics are (1) decision-correlated neural activity showing an initial “featureless” response (equal magnitude regardless of feature value) followed by a decline in the rate of activity, competitive interactions, and a stereotyped excursion of the “winning” representation (e.g., Dorris and Glimcher, 2004; Sugrue et al., 2004; Ipatov et al., 2006; Thomas and Pare, 2007; Churchland et al., 2008); (2) a fixed level of decision-selective activity at the time of the decision (e.g., Roitman and Shadlen, 2002; Churchland et al., 2008); and (3) psychometric and chronometric curves, where accuracy and decision time decrease and increase respectively as a function of task difficulty (see Section 3.1 and Figure 3) and decision times are in the hundreds of milliseconds range (e.g., Roitman and Shadlen, 2002; Palmer et al., 2005; Churchland et al., 2008; Shen et al., 2010). In the context of cortical processing, the first of these characteristics corresponds to a transition from feedforward dominance to feedback dominance, hypothesized to be a fundamental principle of local-circuit cortical processing (see Douglas and Martin, 2007). As we will see, the rate of this transition controls the SAT in our model. The second characteristic provides the motivation for our study, described above. The third characteristic is implicit in the SAT, on the relevant timescale for perceptual decisions.

We simulated a two-choice visual discrimination task by providing two noisy inputs to the model for 1000 ms. The task was to distinguish the stronger input (the target) from the weaker input (the distractor). While the spatial and temporal profiles of the inputs were constrained by the above data, the task clearly generalizes to other decision tasks, just as the model generalizes to other cortical regions. The neural coding of elapsed time (urgency) was simulated with a piecewise linear function (Figure 2C), where the slope of the function was assumed to reflect subjects’ learned estimate of the time available to respond (see Durstewitz, 2004). The activation of each column was simulated with sigmoid function of its input. Gain modulation was implemented by scaling the slope of the sigmoid by the urgency signal during a given trial (Equation 2). As shown in Sections 3.4, 3.5, and 3.6, this approach permits an analysis of the gain-modulated network in trials without gain modulation, where urgency is omitted and the slope of the sigmoid can be set to any value spanned by the scaled slope under gain modulation.

We ran 1000 trials across a range of task difficulties and rates of buildup of urgency (Section 2.3). Task difficulty was controlled by the mean similarity of the input signals, ranging from highly distinguishable (90% similar) to indistinguishable (100% similar) on average (Equation 4). Ideal observer analysis of a population of target and distractor-selective columns was used to determine the timing and accuracy of target discrimination on each trial (Section 2.4).

2.1 THE MODEL

The network is a fully connected recurrent rate model with $N = 100$ nodes, each representing a spatially clustered population of neurons with similar response characteristics (effectively, a cortical column). The firing rate of each population represents the proportion of its neurons emitting a spike at any moment in time (Wilson and Cowan, 1972; Gerstner, 2000). The state of each node $i$ is described by

$$\tau_v \frac{dv_i(t)}{dt} = -v_i(t) + \sum_j W_{ij} r_j(t) + h_i(t) + s_i(t),$$

where the phenomenological state variable $v$ is interpreted as the average membrane potential of each neuron in the column (Amari, 1977; Cremers and Herz, 2002), $\tau_v = 20$ ms is the average membrane...
The intercolumnar interaction structure $W$ is a Gaussian function of the spatial distance between columns arranged in a ring, where excitation-dependent inhibition is provided by subtracting a constant $C$ from this shift-invariant weight matrix (Amari, 1977; Trappenberg and Standage, 2005), depicted in Figure 1A. The strength of interaction between any two columns $i$ and $j$ is thus given by

$$W_{ij} = \Delta x \cdot \gamma_{ij} \left( e^{-dx/2\sigma^2} - C \right)$$  (3)

where $d = \min(i - j, 2\pi - i + j)$ defines distance in the ring, $\Delta x = 2\pi/N$ is a scale factor, and $\gamma_{ij} = 100$ determines the strength of intrinsic (recurrent) activity. Constants $\sigma = 0.75$ mm and $C = 0.5$ support population codes consistent with tuning curves in visual cortex (Mountcastle, 1997; Sompinsky and Shapley, 1997).

### 2.2 Simulated Two-Choice Decision Task

To simulate a reaction time version of a two-choice visual discrimination task, Gaussian response fields (RF) were defined for all columns $i$ by $RF_i = e^{-dx/2\sigma^2}$, where $d$ and $\sigma$ are given above for the intercolumnar interaction structure $W$. Each column $i$ received selective input $s_i = s_i^t + \mu_i^s$ for time $T = 1$ s (the stimulus interval). Columns 25 (the target column) and 75 (the distractor column) were maximally responsive to $s_i^t$ and $s_i^d$ respectively, i.e., the RF centers of the selective inputs were 180° apart in the ring network. Spike response adaptation in upstream visually responsive neurons was modeled by a step-and-decay function (Trappenberg et al., 2001; Wong et al., 2007)

$$\mu(t) = \begin{cases} \gamma_{p} - \gamma_{p} \frac{\mu_{in}}{\mu_{in}} e^{-(t-t_{rel})/\tau_{p}} + \gamma_{p} \gamma_{p} / \mu_{in} & \text{for } t > t_{rel} \\ 0 & \text{for } t \leq t_{rel} \end{cases}$$  (4)

where $\gamma_{p} = 75$ determines the initial strength of input at the target and distractor columns, $\mu_{in} = 3$ determines the asymptotic input strength, $\tau_{p} = 25$ ms determines the rate of input decay, and $t_{rel} = 50$ ms is a visual response delay (Thomas and Pare, 2007). Constant $\gamma_{p}$ was set to 1 for the target and to $\gamma_{p}$ for the distractor, where $0.9 \leq \gamma_{p} \leq 1$ determined target-distractor similarity. The strength of $s_i^t$ and $s_i^d$ respectively was scaled by RF at each column according to its proximity to the target and distractor columns. In noisy simulations, Gaussian noise with mean and SD $\mu$ was added to $s_i^t$ and $s_i^d$ (Salinas and Abbott, 1996). Our use of the same value of $\sigma$ for the (extrinsic) RFs and the (intrinsic) lateral interaction structure $W$ is consistent with the feedforward multiplication of accumulators by Gaussian input signals in the multiple-choice decision task of McMillen and Behseta (2010), shown by these authors to be required for asymptotically optimal hypothesis testing. Simulations were run with Euler integration and timestep $\Delta t = 1$ ms. A 200-ms equilibration period was used. Mean input to the target and distractor columns is shown in Figure 1B.

### 2.3 Gain Modulation by the Urgency Signal

The urgency signal was simulated with a piecewise linear function

$$U(t) = \begin{cases} U_{\text{max}} / \tau_{p} \cdot t & \text{for } t \leq \tau_{p} \\ U_{\text{max}} / \tau_{p} & \text{for } t > \tau_{p} \end{cases}$$  (5)

where $U(t)$ is normally distributed random noise with mean and SD $\mu$.

FIGURE 2 | (A) Sigmoid gain function with different values of the slope parameter $\beta$. Lighter shades of gray correspond to smaller values of $\beta$. (B) Network response (without gain modulation) to a single stimulus for each value of $\beta$ in (A) above. Curves show network activation at the end of the trial. The simulation was identical to the decision task, but noise was omitted for clarity and only one stimulus was used, centered on column 50 (indicated by the arrow). (C) Urgency signal $U(t)$ building up over 1000 ms (solid), 750 ms (dashed), and 500 ms (dotted). Under gain modulation, $\beta$ was scaled by $U(t)$ during each trial (see Equation 2, Section 2), akin to a transition from light gray to black in (A,B) with increasing urgency.
where \( U_{\text{max}} = 0.5 \) and \( \tau_p \in [500, 750, 1000] \) ms determines time over which the signal increases toward \( U_{\text{max}} \), depicted in Figure 2C. Gain modulation was implemented by multiplying the slope parameter \( \beta = 0.0275 \) of the columnar gain function by \( 1 + U(t) \) (Equation 2 above).

### 2.4 Determining the Timing and Accuracy of Discrimination

Signal detection theory (Green and Swets, 1966) was used to quantify the degree to which an ideal observer of network activation could discriminate the target from the distractor, estimating the separation of the distributions of target and distractor-selective rates at successive 1 ms intervals. Signal detection theory is commonly applied to electrophysiological recordings under conditions in which a target stimulus is inside and (on separate trials) outside a neuron's response field, averaged over all trials (Thompson et al., 1996; Thomas and Pare, 2007). Because we can observe all the activity in the model, we applied this method to a population of target and distractor-selective columns on each trial. Each population \( p = 25 \) included the target and distractor columns plus the adjacent 12 = \( \sigma / 2 \pi N \) columns on each side of these response field centers. Receiver operating characteristic curves (ROC) were calculated from the mean rates of these populations, determining mean discrimination for each level of task difficulty and urgency signal \( U(t) \). The area under the ROC (AUROC) quantifies the separation of the distributions of target and distractor activation (see Thompson et al., 1996). The probability of discrimination was quantified by a least squares fit of the AUROCs to a cumulative Weibull function

\[
w(t) = c - (c - d) \cdot e^{-t t/eta^2}
\]

where \( t \) is the time after stimulus onset, and \( a, b, c, \) and \( d \) are fitted parameters: \( a \) is the time at which the function reaches 63% of its maximum, \( b \) is the slope (shape parameter), and \( c \) and \( d \) are the upper and lower limits of the function respectively. Parameter \( c \) quantifies discrimination magnitude and is typically close to 1 (separate distributions of target and distractor activation at the end of a trial), whereas \( d \) is typically close to 0.5 (overlapping distributions at the beginning of a trial, see Figures 4B,C). Because either target or distractor activation could dominate the network on any given trial (correct and error trials respectively), the AUROCs could be fit with increasing or decreasing Weibull functions \( w \). On error trials (decreasing function), \( a \) in Equation 6 refers to the time at which \( w \) reached 63% of \( 1 - \min(w) \), and \( c \) and \( d \) are the lower and upper limits respectively. The time at which \( w \) reached 0.75 was considered the discrimination time (Thompson et al., 1996; 0.25 on error trials). The resulting decision times were averaged over all trials to determine the speed of decision making for each task difficulty and urgency \( U(t) \). Trials on which \( w \) reached neither 0.75 nor 0.25 were considered “no decision” trials.

### 3 RESULTS

We begin the Section 3 by showing that gain modulation of the network by a growing urgency signal produces the SAT (Section 3.1), where decision-selective activation at decision time is approximately constant across all task conditions, referred to as reaching a fixed threshold (Section 3.2). We subsequently explain these results in terms of the network’s dynamics. Before doing so, it is useful to define some terminology. We define the decision variable as the difference between the activation of the target and distractor columns, and we define the time over which the noise-free model can calculate the decision variable as the network’s effective time constant of integration \( \tau_{\text{lin}} \) (Section 3.3). In Section 3.4, we show that as the urgency signal builds up, the network progresses through processing stages supporting a range of integration times, dominated by leakage early in each trial and by feedback inhibition later on (Usher and McClelland, 2001; Bogacz et al., 2006). The latter entails an acceleration of the decision variable, which we refer to as amplification. Note that our use of this term refers to the decision variable only, not to the network processing more generally. In Section 3.5, we show that the within-trial progression from leakage to inhibition-dominated processing allows the network to take advantage of dynamics inherently suited to different stages of the decision process, distinguishing the network from earlier models that produced the SAT with a constant within-trial signal (variable between blocks of trials). In Section 3.6, we take a dynamic systems approach, showing that our numeric explanation corresponds to a bifurcation between dynamic regimes. We analytically calculate the time constant of the linear approximate system, referred to as \( \tau_{\text{lin}} \), which undergoes the same qualitative progression as \( \tau_{\text{lin}} \) in Section 3.4. Note that in simulations and analysis without gain modulation, we refer to the network as the fixed-gain network to the slope parameter of its gain function as \( \beta \). Thus, for a given value of urgency \( U(t) \) in the gain-modulated network, \((1 + U(t)) \beta = \hat{\beta} \) in the fixed-gain network. In Section 3.7, we show that the network earns more reward per unit time than a fixed-gain network with \( \hat{\beta} \) tuned for best performance.

#### 3.1 Speed and Accuracy of Decisions

For all rates of buildup of urgency \( U \), decisions took longer and became less accurate with increasing task difficulty. The gain-modulated network thus produced typical psychometric and chronometric curves, demonstrating speed, and accuracy of decisions consistent with behavioral data (e.g., Roitman and Shadlen, 2002). Longer buildup of \( U \) resulted in slower, more accurate decisions for a given task difficulty (Figure 3). Under the same conditions, shorter buildup resulted in faster, less accurate decisions. The network thus produced the SAT. Of note, with lower task difficulty (90–97% similarity), the network showed another advantage of dynamics inherently suited to different stages of the decision process, distinguishing the network from earlier models of decision circuits (Wong and Wang, 2006).

#### 3.2 Target-Selective Activation in the Network

Consistent with neural data (Hanes and Schall, 1996; Churchland et al., 2008), target-selective activation is approximately constant at decision time across all task conditions (between 0.365 and 0.385; Figure 4A). It also reaches a common maximum rate across all conditions (Figures 4B,C), as seen in LIP during visual tasks (Roitman and Shadlen, 2002; Huk and Shadlen, 2003; Churchland et al., 2008). These two findings demonstrate a subtle but important distinction. We used ideal observer analysis to determine stimulus discrimination, so the constant level of activation at decision time...
demonstrates that a downstream network could employ a fixed threshold when making decisions based on network activity (e.g., the superior colliculus reading out LIP activity). The stereotyped maximum rate of selective activation demonstrates that the network could also employ a fixed threshold to make decisions on its own, i.e., without an observer of its activity. Our results therefore demonstrate that gain modulation by the encoding of urgency can account for the SAT with a fixed threshold, whether a downstream network is reading out the modulated network or if the modulated network has the “final say” on the decision itself. Using a constant threshold to determine speed and accuracy produced similar results to those produced by ideal observer analysis (not shown).

3.3 THE EFFECTIVE TIME CONSTANT OF INTEGRATION OF THE NETWORK

The time over which a recurrent network can accumulate evidence (its effective time constant of integration $\tau_{\text{eff}}$) can be controlled by parameters determining the strength of network dynamics (Wang, 2002; Wong and Wang, 2006). Above and below an optimal regime, $\tau_{\text{eff}}$ is progressively shortened (Wang, 2008), dominated by amplification and leakage of accumulated evidence respectively (Usher and McClelland, 2001). Larger values of $\tau_{\text{eff}}$ favor accuracy because the network can accumulate evidence for longer. Smaller values favor speed. The ability of the network to trade speed and accuracy as a function of urgency can thus be understood by considering the effect of urgency on its integration time.

We approximated $\tau_{\text{eff}}$ under gain modulation by running a noise-free trial for each $U$ and task difficulty. In each of these trials, we integrated the difference between the firing rates at the target and distractor columns, where $\tau_{\text{eff}}$ was the time at which this difference (the decision variable) stopped growing (precision $10^{-4}$). Longer buildup of $U$ yielded longer integration times (Figure 5A). Target-selective rates reached a stereotyped maximum (−0.85) at $\tau_{\text{eff}}$ for all $U$ and task difficulties. These results are not surprising after the results shown in Figures 3 and 4, but they demonstrate an important principle: slower (faster) buildup of $U$ facilitated longer (shorter) accumulation of evidence under gain modulation, precisely the requirement for the DDM to trade speed and accuracy. We build on this principle below.
3.4 Urgency Controls the Speed of Transitions through Processing Stages with Different Effective Time Constants

The above calculation of the network’s effective time constant $\tau_{\text{eff}}$ for each urgency condition explains why the model produces the SAT: slower buildup of $U$ furnishes a longer time constant. But it does not explain how. The mechanism by which gain modulation controls integration time can be understood by measuring $\tau_{\text{eff}}$ in the network without gain modulation (the fixed-gain network) for different values of the slope parameter $\hat{\beta}$. Here, the values of $\tau_{\text{eff}}$ can be thought of as successive snapshots of the network’s effective time constant under gain modulation. Consistent with earlier analysis (Wang, 2008), $\tau_{\text{eff}}$ decreased as $\hat{\beta}$ deviated from the value supporting the longest $\tau_{\text{eff}}$ (Figure 5B), that is, above and below this optimal value, the decision variable was increasingly dominated by amplification and leakage respectively.

Under gain modulation, the network progresses through all these processing stages on each trial. As such, the decision variable is dominated by leakage early in the trial when urgency is low and is amplified later in the trial when urgency is high (see Figure 6B). $\tau_{\text{eff}}$ is thus progressively lengthened over the early part of the trial and contracted later on, terminating the decision process. This progression corresponds to a transition from left to right in Figure 5B. In effect, slower buildup of urgency allows the network to spend more time in processing stages with a longer time constant.

Note that our method of calculating $\tau_{\text{eff}}$ is conservative. For example, time constants are often taken at some percentage of the completion of a process, such as half-life. With and without gain modulation (Figures 5A,B respectively), the computed values of $\tau_{\text{eff}}$ are consistent with earlier approximations of cortical network time constants of up to several seconds (Wang, 2002). This would remain the case if $\tau_{\text{eff}}$ was taken at half rise time. Note also that this theoretical construct is not the same thing as decision time, i.e., the decision variable is saturating for much of $\tau_{\text{eff}}$ and a downstream network could read out the decision before saturation.

3.5 A Progression from Leakage to Amplification of the Decision Variable

The progression from leakage to amplification of the decision variable with the buildup of urgency can be further understood by observing the activity in the fixed-gain network during the decision task for different values of $\hat{\beta}$. Mean activation over the target and distractor populations on a noise-free trial is shown for one task difficulty (97% similarity) in Figure 6. With low gain, the network distinguishes one signal from the other, but cannot accumulate much of the difference between the signals as the trial progresses (Figure 6B, lightest gray curves). As such, the network is capable of functioning as a noise filter, recognizing a difference between input signals, but leakage and inhibition are soon balanced (Usher and McClelland, 2001). With increased gain, the network integrates the difference between signals over the full trial, approximating the DDM, as evidenced by the near-linear increase of the decision variable (medium gray). With a further increase in gain, the network amplifies an integrated difference between inputs (dark gray). With high gain, the network quickly amplifies a small difference, demonstrating dynamics suitable for categorical choice (black). The precise correspondence between the slope parameter $\hat{\beta}$ of the gain function and each of these stages depends on the mean difference between signals, but other task difficulties yield similar curves.

 Whereas the fixed-gain network implements a single regime for each value of $\hat{\beta}$, the gain-modulated network transitions through these regimes on each trial, where the rate of transition is determined by the timecourse of the urgency signal $U$. Thus, with gain modulation, the network smoothly progresses through a series of processing stages implementing noise filtering, difference integration, difference amplification, and selection. As such, the network begins each trial conservatively (dominated by leakage), but becomes less so as information is accumulated. The slower the buildup of $U$, the longer the network spends in more conservative stages, enabling higher accuracy at the expense of speed. This progression is depicted by the vertical arrow in Figure 6B. The outcome of the different rates of progression can be seen in the mean target and distractor-selective activation under gain modulation shown in Figures 4A,B, where activation diverges more slowly with slower buildup of $U$. Figure 3 shows the resulting SAT.

3.6 Non-linear Dynamic Analysis of the Model

The above simulations demonstrate the SAT with a fixed neural threshold and provide an intuitive picture of network dynamics with growing urgency. In this section, we take a non-linear dynamics approach to formally characterize this picture.

3.6.1 Two regimes for decision making

From a dynamic systems point of view, the accumulation of evidence in the network is the evolution of a dynamic system from an initial state to an attractor corresponding to the target or the distractor. The evolution is determined by the structure of the steady states of the system (Strogatz, 2001). In our model, the slope parameter $\beta$, urgency signal $U$, and the target-distractor similarity $\gamma_{\text{ad}}$ determine the steady states of the system defined by Equation 1. By setting the right hand side of Equation 1 to zero, we obtain a set of algebraic equations, the solution of which gives the steady states. Based on the steady state of the system, the decision process can be classified according to two regimes: in regime 1, the system evolves directly from the initial state to a single attractive stable steady state (see Figure 7A). In regime 2, the system is driven away from an unstable steady state to one of two stable steady states (see Figure 7B).
are two regions in the plane of \((1 + U)\beta\) over \(\gamma_{ext}\). The system has one stable steady state in one region and three steady states in the other.

Thirdly, the evolution from the initial state to the stable steady state is determined by the structure of the steady states. In regime 1, the system evolves directly from the initial state to the single stable steady state of the target. The dynamics in the vicinity of this stable state determine the characteristics of the decision. In regime 2, the initial firing rate of the target population equals that of the distractor population (see Figure 4), so the initial state is in the vicinity of the two-bump unstable steady state. Therefore, the evolution from the initial state to the stable steady state is determined by the dynamics in the vicinity of the unstable steady state.

3.6.2 Regimes for accuracy and decisiveness

As described above, the decision ensues with the evolution of the system to the stable steady state. The dynamics in the vicinity of the steady state (the stable steady state in regime 1 and the unstable steady state in regime 2) thus determine task performance, such as speed, accuracy, and decisiveness (whether or not a decision is made). We have used signal detection theory to determine the decision on each trial, where the AUROC is used to estimate the separation of the distributions of target and distractor-selective activation. On any given trial, the activation of the noisy system fluctuates around the rates of the noise-free system. Therefore, the overlap of the two distributions decreases (and thus the AUROC increases) with the increase of the difference between the target and distractor-selective activation in the noise-free system. In regime 1, if the difference between the two bumps of the stable steady state is small [i.e., a low value of \((1 + U)\beta\) and a high value of \(\gamma_{ext}\)], the two distributions overlap too much to be discriminated and the network cannot make a decision. However, if the difference between the two bumps of the stable steady state is large enough to be discriminated, the network cannot make errors.

In regime 2, the system is driven away from the unstable steady state to one of the two stable steady states, where the difference between target and distractor-selective activation is large enough to make a decision (see \(\beta = 0.04\) in Figure 6). Because the system is sensitive in the vicinity of the unstable steady state, it may be driven in the wrong direction by noise, i.e., it can make errors in regime 2. Thus, the network is decisive, but makes some mistakes in regime 2, whereas it either makes correct decisions or no decision at all in regime 1.

3.6.3 The time constant of the approximate linear system

In the vicinity of the steady state, the dynamic system (Equation 1) can be linearized as

\[
v(t) = \bar{v} + \sum c_ie^{\lambda t}\mu_i
\]

where \(\bar{v}\) is interpreted as the mean membrane potential, \(\bar{v}\) is the steady state of the system, \(\mu_i\) is the \(i\)th eigenvector, \(\lambda_i\) is the \(i\)th eigenvalue, and \(c_i\) is the projection of the difference between the initial state and the steady state, defined by

\[
c_i = \frac{\mu_i^T(\bar{V} - \bar{v})}{\mu_i^T\mu_i}
\]
In regime 1, the eigenvalues for the stable steady state are negative, and the evolution of the system along the invariant manifold tangent to the eigenvector corresponding to the largest eigenvalue (i.e., the one closest to 0) determines how slowly the system reaches the stable steady state. Therefore, the absolute value of the reciprocal of the largest eigenvalue can be used to approximate the time it takes for the system to reach the stable steady state and is defined as the time constant. In regime 2, we consider the time it takes for the system to evolve away from the unstable steady state. The reciprocal of the largest positive eigenvalue approximates the time over which the system departs from the unstable steady state of the invariant manifold tangent to the eigenvector corresponding to the largest eigenvalue. Therefore, the absolute reciprocal of the largest eigenvalue of the stable steady state in regime 1 and the unstable steady state in regime 2 depicts the time over which the system makes a decision and is denoted $\tau_{\text{inst}}$.

For a given target-distractor similarity $\gamma_{\text{ext}}$, the system operates in regime 1 or regime 2, depending on the value of $\vec{\beta} = (1 + U) \cdot \vec{\beta}$ (Figure 7). The time constant $\tau_{\text{inst}}$ is shown for three values of $\gamma_{\text{ext}}$ in Figure 8, where for each curve, the left side of the discontinuity shows the time constant of the stable steady state in regime 1, and the right side shows the time constant of the unstable steady state in regime 2. These curves show the same qualitative increase and subsequent decrease with increasing of $\vec{\beta}$ shown for integration times in Figure 5B, where more difficult tasks have longer time constants. The slight exceptions to these characteristics occur in the vicinity of the bifurcation, where the time constant is undefined because the eigenvector is zero at the bifurcation point, but the progression through processing stages with different time constants described in Sections 3.3 and 3.5 is clear. Notably, the time constants in Figures 5 and 8 peak at approximately the same value of $\vec{\beta}$.

### 3.6.4 The dynamics of decision making with growing urgency

With growing urgency, decision processing under gain modulation can be described according to the above two regimes. In the early stages of a decision, the system operates in regime 1 because the urgency signal is low. The system has only one stable steady state with activation bumps centered at the target and distractor columns. As the urgency signal grows, the target and distractor-selective activation in the steady state gradually increases and decreases respectively (see Figures 9A–C). This changing stable steady state is tracked by the system and consequently the target and distractor-selective activation in the network gradually increases and decreases respectively before the urgency signal exceeds the bifurcation threshold (Figure 7C). If the urgency signal does not cross the bifurcation threshold, the system will approach the stable steady state of the final urgency signal. If the difference between the target and distractor-selective activation is large enough, the system makes a correct decision, otherwise, it makes no decision. Once the urgency signal exceeds the bifurcation threshold, the system operates in regime 2 and the stable steady state splits into three steady states, one unstable and two stable (see Figures 9D–F). At the same time, the state of the system, which tracks the stable steady state in regime 1 and whose target-selective activation is stronger than the distractor-selective activation, falls into the vicinity of the unstable steady state in regime 2. Driven away from the unstable steady state, the system evolves to one of the stable steady states (corresponding to the target or the distractor) and makes a decision.

In the fixed-gain network, the decision process occurs either in regime 1 or in regime 2, depending on the slope parameter $\vec{\beta}$ and the target-distractor similarity $\gamma_{\text{ext}}$. For distinguishable tasks under gain modulation, if the urgency signal is big enough to cross the bifurcation threshold ($0.95 < \gamma_{\text{ext}} < 1$), the progression from regime 1 to regime 2 allows the network to begin regime 2 in a state closer to the target attractor than would be the case in the fixed-gain network with slope parameter $\vec{\beta}$ equal to $1 + U(\vec{T}) \cdot \vec{\beta}$, where $\vec{T}$ is the time at which $U$ crosses the bifurcation threshold. This advantageous position of the network state formally characterizes the progression described in Section 3.5, where early noise filtering allows late amplification of a high-quality decision variable. As described in Section 3.6.3, the progression stretches the time constant $\tau_{\text{inst}}$ as the system moves through regime 1, before contracting it in regime 2 on the way to the stable steady state of the target or the distractor. Speed and accuracy are traded because the time constant $\tau_{\text{inst}}$ and the decision variable are larger at decision time with slower buildup of $U$ (not shown). When the decision occurs in regime 1, the decision variable is larger at decision time with faster buildup of $U$, but accuracy is not compromised because the network cannot make errors.

### 3.7 Optimal decision making

The above analysis shows that the bifurcation between regime 1 and regime 2 under gain modulation puts the network in a state closer to the target attractor when it enters regime 2 than would be the case in the fixed-gain network with slope parameter $\vec{\beta}$ equal to $1 + U(\vec{T}) \cdot \vec{\beta}$ at the time of the bifurcation $\vec{T}$. This analysis suggests that gain modulation by the urgency signal may produce more accurate decisions per unit time than the fixed-gain network. To investigate this possibility, we calculated the reward rate over a full block of 6000 trials (1000 trials for six values of target-distractor similarity $\gamma_{\text{ext}}$) under gain modulation for each of the above rates of buildup of $U$. Because the urgency signal simulates...
This finding is instructive in several regards. Earlier work showed that a spatially non-selective signal, variable between blocks of tri-
alys, but constant within each trial, could potentially produce the SAT with a fixed threshold (Bogacz et al., 2006; Furman and Wang, 2008). This approach is equivalent to setting $U$ to a fixed value between trials in our model and could be instantiated by goal-directed persistent activity in higher association cortical areas (see Goldman-Rakic, 1995; Wang, 2001). This mechanism is plausible, though we are unaware of any data showing the rate of persistent activity to vary systematically between trials or blocks of trials, as would be required. There is a growing body of data showing the neural encoding of elapsed time relative to learned inter-
vals (see Durstewitz, 2004), previously correlated with decisions (Churchland et al., 2008) and proposed here to control the SAT.

The analysis in Section 3.6 and the calculation of reward rate in this section show that a within-trial signal is optimal in our model, though we expect within-trial and between-trial gain modulation to play complimentary roles in decision making and cognitive func-
tion more generally (see Section 4.4).

4 DISCUSSION

Our model offers a candidate neural mechanism for the SAT. We propose that gain modulation by the encoding of urgency controls the time constant of cortical decision circuits “on the fly.” The rate of buildup of urgency determines how long the circuit integrates evidence before the decision variable is amplified. Longer (shorter)
4.1 A NEURAL MECHANISM FOR TIME-VARIANT DRIFT DIFFUSION WITH A FIXED THRESHOLD

Our neural model is grounded in abstract, mathematical models that have been instrumental in characterizing decision processes. Sequential sampling models are based on the premise that evidence is integrated until it reaches a threshold level (see Smith and Ratcliff, 2004). Because evidence may be incomplete or ambiguous and neural processing is noisy, temporal integration provides an average of the evidence, preventing decisions from being made on the basis of momentary fluctuations in either the evidence or processing. The longer the integration time, the better the average (see Bogacz, 2007). In two-choice tasks, integrating the difference between the evidence favoring each option implements the DDM, known to yield the fastest decisions for a given level of accuracy and the most accurate decisions for a given decision time (see Bogacz et al., 2006). The DDM thus optimizes speed and accuracy for a given threshold. The SAT can be achieved by varying the threshold, a principle suggested to be instantiated in the brain (Gold and Shadlen, 2002).

The DDM has been augmented with a time-variant mechanism similar in principle to our use of urgency (differences between the models are described below). In the model by Ditterich (2006b), the decision threshold is lowered over the course of each trial. This approach is functionally equivalent to an increasing multiplication of the evidence as the trial progresses, demonstrated to earn more reward per unit time than the standard DDM in a two-choice task with no explicit deadline (Ditterich, 2006a). The time-dependent multiplication of evidence permits the effect of urgency with a fixed threshold, so this abstract model is consistent with neural data in that regard. Although the SAT was not a focus of these studies, varying the rate of either time-dependent mechanism would effectively trade speed and accuracy.

Neural models have addressed the possible mechanisms underlying the above mathematical models, several of which have been shown to be equivalent to the DDM under biophysical constraints. In these models, the subtractive operation is implemented by mutual inhibition between neural populations selective for each option of a decision (Bogacz et al., 2006), a ubiquitous neural process that scales naturally with the number of options (Usher and McClelland, 2001). Recurrent processing allows slow integration, where network dynamics yield effective time constants much longer than those of contributing biophysical processes (e.g., the time constants of synaptic receptors; Wang, 2002). This neural framework accounts for wealth of neural and behavioral data (see Schall, 2001; Gold and Shadlen, 2007; Wang, 2008). Varying a threshold firing rate will trade speed and accuracy in these models, but, as described above, it conflicts with experimental data (see Schall, 2001).

Our model trades speed and accuracy with a fixed threshold by exploiting the time constant of recurrent networks (Sections 3.3 and 3.6.3). Previous work showed that biophysically based parameters determine an optimal processing regime (Wang, 2002; Wong and Wang, 2006), above and below which the time constant is monotonically shortened (Wang, 2008), dominated by inhibition and leakage respectively (Usher and McClelland, 2001; Bogacz et al., 2006). In these studies, networks were tuned to a single set of parameters that were chosen for best performance. This configuration was then used in a decision task. Unlike these models, our network employs a range of time constants on each trial, where speed and accuracy are traded according to the rate of progression from leakage to inhibition-dominated processing (Sections 3.4 and 3.5). The rate of progression is determined by the urgency signal. Because the network passes through the same processing stages in all cases, its activity follows the same trajectory and decisions can be made with a fixed threshold. In effect, faster (slower) buildup of urgency contracts (expands) the progression in time, but nothing else changes.

4.2 BIOLOGICAL CORRELATES OF THE MODEL

We have used a network belonging to a class of local-circuit models (Wilson and Cowan, 1973; Amari, 1977) widely used to simulate cortical processing of continuous feature values such as spatial location (Camperi and Wang, 1998; Standage et al., 2005). These models are referred to by a number of names, including dynamic neural fields (Trappenberg, 2008), line attractor networks (Funran and Wang, 2008) and basis function networks (Pouget et al., 2000). The model’s foundations are based on a columnar structure where inhibition is broadly tuned and the probability of lateral excitatory synaptic contact is normally distributed (see White, 1989; Abeles, 1991; Goldman–Rakic, 1995).

We have modeled subjects’ estimates of the passage of time with a piecewise linear function, where different slopes correspond to different urgency conditions (Figure 2C). While this first approximation is clearly simplistic, it is supported by neural data showing approximately linear ramping that reaches a common peak around the time of an anticipated event (see Durstewitz,
In reaction time tasks with a deadline (Schall and Hanes, 1993; McPeek and Keller, 2004; Thomas and Pare, 2007), such activity would provide an explicit encoding of the urgency to respond. Even in reaction time tasks without a deadline, it is common to constrain the timing of reward to discourage fast reaction times (Roitman and Shadlen, 2002; Huk and Shadlen, 2005), motivating subjects to self-impose deadlines that limit the time between trials (and thus rewards). Neural correlates of temporal estimates have been described in posterior parietal cortex (Leon and Shadlen, 1993; Jansen and Shadlen, 2005), prefrontal cortex (Genovesio et al., 2006), premotor cortex (Mita et al., 2009), and the mid-brain superior colliculus (Thevarajah et al., 2009) among other structures. These data suggest that temporal coding mechanisms can be more complex than linear ramping activity, but the model is by no means limited to the linear case. For example, in the DDM with a collapsing threshold, best performance was achieved with a logistic function of time, rather than a linear function (Ditterich, 2006b). Whether and how different urgency signals affect the model is left to a follow up study.

Neural mechanisms that may underlie gain modulation include recurrent processing of spatially non-selective input (Salinas and Abbott, 1996), voltage-dependent dendritic non-linearities (Mel, 1993; Larkum et al., 2004), and changes in cellular input–output relationships caused by temporal correlations in input activity (Salinas and Sejnowski, 2001), background noise (Chance et al., 2002; Prescott and Konink, 2003; Higgs et al., 2006), and other factors leading to variable conductance states (Destexhe et al., 2003). Our method of gain modulation was meant to abstract over such mechanisms. Note that alternative methods of gain modulation lead to similar results, including the multiplication of network activity by the urgency signal, and the urgency-dependent increase in the strength of recurrent connections (not shown).

4.3 Differences with Earlier Time-variant Models of Decision Making

While conceptually similar to Ditterich’s (2006a) time-variant DDM, our network model differs in a crucial respect: the evolving decision variable is subject to gain modulation, not just the instantaneous evidence. Consider the DDM performing a two-choice decision task. As above, let $s'$ and $s''$ refer to noisy evidence for the target and distractor respectively. At any instant, the difference between the evidence for each option is $x(t) = s'(t) - s''(t)$, which is integrated over time. Let $X$ refer to the running total (the decision variable). The time at which the absolute value $|X|$ exceeds a threshold $\theta > 0$ is the decision time. If $X$ is positive at the decision time, the target is chosen. If $X$ is negative, the distractor is chosen. We may therefore express the DDM as

$$\frac{dX}{dt} = s'(t) - s''(t); \quad |X| \leq \theta. \quad (9)$$

In the time-variant DDM (Ditterich, 2006a), $s'$ and $s''$ are multiplied by an increasing temporal signal similar to the urgency signal $U$. Thus, Ditterich’s model may be expressed as

$$\frac{dX}{dt} = U(t) \cdot \left[ s'(t) - s''(t) \right]; \quad |X| \leq \theta. \quad (10)$$

Like Equation 10, the input signals to our network model are subject to an increase in gain, but so is the recurrent processing of the decision variable. The subtractive operation is supported by recurrent inhibition. We may thus express our model as

$$\frac{dX}{dt} = \alpha \cdot U(t) \cdot X(t) + U(t) \cdot \left[ s'(t) - s''(t) \right]; \quad |X| \leq \theta, \quad (11)$$

where $\alpha$ is a (positive) scale factor. The practical difference between the two models is the time of arrival of the evidence subject to strong amplification. In Equation 10 (and in Ditterich’s model), an increasing urgency signal gives greater weight to later evidence than earlier evidence because only the input is amplified. In Equation 11 (and in our network model), there is a transition from a heavier weighting of the input to a heavier weighting of the decision variable, similar to the transition from extrinsic to intrinsic processing hypothesized to be a fundamental principle of local-circuit cortical processing (see Douglas and Martin, 2007). The urgency signal governs the rate of this transition.

The implications of the difference between the two models can be seen in Figure 11A for a noisy trial with 99% target-distractor similarity, where Equations 10 and 11 were given the same inputs received by the target and distractor columns in the network, $U_{\text{max}} = 10$ (Equation 5) and $\alpha = 1/1000$. Equation 11 makes different decisions for different rates of urgency buildup. With faster buildup, the model effectively ignores later evidence (see figure caption). In contrast, Equation 10 is always dominated by its inputs. This feedforward dominance is clearly shown in Figures 11B,C, where the evidence for the target and the distractor was switched in the fourth and first quartiles of a noise-free trial respectively (see figure caption). An attractive feature of Equation 11 is the explosion of the decision variable (black curves in the figure), alleviating the need for fine tuning of the decision threshold, similar in principle to the subcritical bifurcation in the non-linear diffusion model by Roxin and Ledberg (2008).

While the difference between these time-variant DDMs is clear from Equations 10 and 11 and Figure 11, we do not further investigate the novel DDM introduced by Equation 11 in this paper. Suffice to say, we anticipate that Equations 10 and 11 will produce similar results over a block of trials with constant mean evidence (within each trial), the dominant experimental approach to date (e.g., Roitman and Shadlen, 2002; Thomas and Pare, 2007; Churchland et al., 2008). However, in trials with interference stimuli (Huk and Shadlen, 2005) or changing evidence (Cisek et al., 2009), results will differ due to the timing of amplification. It is worth noting that both models produce error trials that are longer than correct trials, but they do so for different reasons. As elegantly explained by Ditterich (2006b), error trials are longer than correct trials in his model because noise grows faster than drift rate; the lower signal-to-noise ratio later in trials leads to more errors, so error trials are longer on average. Here, error trials take longer because the system has to cross the invariant manifold of the unstable steady state, which takes more time.

Our model also bears conceptual similarities with the “urgency gating” models of Cisek et al. (2009). In their study, mathematical models were compared for their ability to explain data from decision tasks with changing evidence. Under noisy conditions, the
comes (Dorris et al., 2000; Thevarajah et al., 2010). Within-trial varying the initial strength of the network on each trial (the initial Trial-to-trial modulation could be implemented in our model by processing occurs on longer timescales as well, providing a mechanism for instantiating the approach of Gold and Shadlen (2002). The former specifies a decision threshold for the DDM for all trials of an experiment (or some set of decisions). The latter adjusts the decision threshold on a within-trial basis, lowering it over the course of each trial. Although our neural model uses a within-trial approach, it offers a time-variant mechanism that in principle, can flexibly implement either or both approaches. The gain-modulated network began and ended each trial in extreme regimes dominated by leakage and inhibition respectively. These rough parameters account for the SAT, but modulation of cortical processing occurs on longer timescales as well, providing a mechanism for instantiating the approach of Gold and Shadlen (2002). Trial-to-trial modulation could be implemented in our model by varying the initial strength of the network on each trial (the initial value of $\beta$) depending on previous choices and their reward outcomes (Dorris et al., 2000; Thevarajah et al., 2010). Within-trial and between-trial modulation are both potentially supported by the different timescales of dopamine signals (see Schultz, 2007). Dopamine is extensively correlated with reward (see Schultz, 2006) and can modulate gain in cortical circuitry (see Seamans and Yang, 2004). We thus envision trial-to-trial and within-trial modulation playing complementary roles in decision making.

4.4 Flexible Modulation of Decision Circuitry on More Than One Timescale

Ultimately, the modulation of decision circuitry is likely to occur on more than one timescale. Two such timescales are captured by the mathematical models of Gold and Shadlen (2002) and Ditterich (2006b). The former specifies a decision threshold for the DDM for all trials of an experiment (or some set of decisions). The latter adjusts the decision threshold on a within-trial basis, lowering it over the course of each trial. Although our model uses a within-trial approach, it offers a time-variant mechanism that in principle, can flexibly implement either or both approaches. The gain-modulated network began and ended each trial in extreme regimes dominated by leakage and inhibition respectively. These rough parameters account for the SAT, but modulation of cortical processing occurs on longer timescales as well, providing a mechanism for instantiating the approach of Gold and Shadlen (2002). Trial-to-trial modulation could be implemented in our model by varying the initial strength of the network on each trial (the initial value of $\beta$) depending on previous choices and their reward outcomes (Dorris et al., 2000; Thevarajah et al., 2010). Within-trial and between-trial modulation are both potentially supported by the different timescales of dopamine signals (see Schultz, 2007). Dopamine is extensively correlated with reward (see Schultz, 2006) and can modulate gain in cortical circuitry (see Seamans and Yang, 2004). We thus envision trial-to-trial and within-trial modulation playing complementary roles in decision making.

4.5 Summary and Conclusions

Models of decision circuits have demonstrated that network dynamics determine time constants of integration (Wang, 2002, 2008; Wong and Wang, 2006) and that corresponding processing regimes are subject to modulation (Eckhoff et al., 2009). To date, however, neural models instantiating the DDM have used a single mechanism to control speed and accuracy: the difference between the decision threshold and the level of activity on which the decision variable builds (see Bogacz et al., 2006 for analysis of these models). If sufficiently variable, initial levels of activity could account for the SAT with a constant threshold. Here, we propose another, compatible mechanism. In the context of sequential sampling models, the crucial factor is integration time, control of which is not limited to the difference between initial and threshold levels of activity. In this regard, it is instructive to distinguish between the quality of the decision variable and the rate of neural activation sufficient for the decision. For example, network dynamics force decisions in our model when the target and distractor are identical on average, also shown by earlier models (Wang, 2002; Wong and Wang, 2006). This property is useful because decisions often have deadlines, but the quality of the decision variable is low in these cases.

The notion of urgency in decision making is not new (Reddi and Carpenter, 2000) and is an instance of the concept of hazard rate, or the anticipation of an upcoming event (Luce, 1986; Janssen and Shadlen, 2005). A growing body of experimental data suggests that the encoding of time is as natural a process as the encoding of space (see Durstewitz, 2004; Mauk and Buonomano, 2004; Buhusi and Meck, 2005). When faced with deadlines, either self-imposed or imposed by the environment, it appears we automatically encode the urgency to respond. At least one empirical study has quantified the representation of urgency along these lines, where neural activity was correlated with both the passage of time and subjects’ decisions in a decision task, independent of the evidence (Churchland et al., 2008). Our study proposes a neural mechanism by which integration and urgency are combined: decisions are based on integrated evidence, but integration time is controlled by the representation of urgency.

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