Bio-mimetic Adaptive Force/Position Control Using Fractal Impedance

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Abstract—The ability of animals to interact with complex dynamics is unmatched in robots. Especially important to the interaction performances is the online adaptation of body dynamics, which can be modelled as an impedance behaviour. However, variable impedance control still continues to be a challenge in the current control frameworks due to the difficulties of retaining stability when adapting the controller gains. The fractal impedance controller has recently been proposed to solve this issue. However, it still has limitations such as sudden jumps in force when it starts to converge to the desired position and the lack of a force feedback loop. In this manuscript, two improvements are made to the control framework to solve these limitations. The force discontinuity has been addressed introducing a modulation of the impedance via a virtual antagonist that modulates the output force. The force tracking has been modelled after the parallel force/position controller architecture. In contrast to traditional methods, the fractal impedance controller enables the implementation of a search algorithm on the force feedback to adapt its behaviour to the external environment instead of relying on a priori knowledge of the external dynamics. Preliminary simulation results presented in this paper show the feasibility of the proposed approach, and it allows to evaluate the trade-off that needs to be made when relying on the proposed controller for interaction. In conclusion, the proposed method mimics the behaviour of an agonist/antagonist system adapting to unknown external dynamics, and it may find application in computational neuroscience, haptics, and interaction control.

I. INTRODUCTION

The dynamic dexterity of animals is far beyond the current capabilities of artificial systems, despite their theoretical limitation in information transmission and processing [1]–[4]. An important limitation in state-of-the-art control frameworks is the reduced performance and reliability when dealing with highly variable dynamic interaction (e.g., contacts). Here, a major limitation is the dependence of their stability on an accurate interaction dynamics model; which inherently is not easy to track with the unpredictability of real-world interaction scenarios [5], [6]. Therefore, the identification of a method to overcome such limitation is likely to have a significant impact on the robustness of legged robots such as quadrupeds and humanoids, haptic technologies, exoskeletons, and rehabilitation systems.

One of the theories on how nature has overcome these biological limitations is based on the theory that the body motor control acts as a hierarchical architecture of semi-autonomous controllers [4], [7]. In this type of architecture, each layer is accountable for the stability while accurately executing the behaviour directed from the higher level controller, while at the same time coordinating and verifying the behaviour of lower level controllers. This can be observed starting from the muscular level where each muscle contains structures that can modulate its mechanical impedance [8]–[11]. Moving to a higher level, motor synergies can be identified that co-activate muscles, often across multiple joints, to produce desired body motions [1], [2], [4], [7], [12]. The motor synergies themselves are identified at different hierarchies starting from a single agonist/antagonist behaviour to more complex stereotyped movements that are implemented in the coordination of complex actions, such as balance [4]. In summary, there is a multitude of studies indicating that the motor control modulates the mechanical impedance of the human body to adapt to the task requirements.

The identification of the ability of motor control to modulate the body impedance lead to theories based on the Port-Hamiltonian framework [13]. However, their integration in a complex hierarchical architecture of semi-autonomous controllers is still an open issue. Furthermore, despite interaction control based on the Port-Hamiltonian approach having been proposed in the forms of impedance and admittance control, there are still issues when dealing with variable impedance and the interaction with complex external dynamics.

Impedance and admittance control differ on the methodol-
The Fractal Impedance Controller is based on an attractor that alters its topology between its divergence and convergence phases (Fig. 2a) [15]. During divergence, the controller stiffness is described as a spring centred in the desired position. During convergence, the controller acts as a constant spring centred in the mid-point between the desired position and the maximum displacement ($\tilde{x}_{\text{Max}}$) reached during the divergence phase [15]. Such behaviour is obtained with an algorithm that mimics the electrical equivalent as shown in Fig. 2b. The behaviour during divergence is determined by $Z_{\text{Div}}$, while an additional impedance $Z_{\text{Conv}}$ is added in series for convergence. Thus, the system behaves like having a total impedance equal to $Z_{\text{Tot}} = Z_{\text{Div}} + Z_{\text{Conv}}$. Furthermore, the fractal impedance controller does not have a damping component, which implies that the controller generates a conservative energy field centred in the desired pose. It shall be noted that a damping component can be introduced without affecting stability as long as the desired velocity is equal to zero [15].

This approach has been inspired by the agonist/antagonist muscles and the concept of dynamic primitives, which can be seen as libraries of stereotyped basic behaviours that can be superimposed to achieve complex actions [1], [2], [4], [17], [18]. Specifically, the hypothesis was that it should be possible to embed stability into the control algorithm itself identifying a stereotyped behaviour that could scale with the energy accumulated in the system without compromising stability. In other words, is it possible that what we observe as variable impedance in humans is produced by the scaling of intrinsically stable stereotyped embedded systems?
Following such a change of perspective, the problem is transformed into one of how to embed a smooth trajectory into the attractor of the impedance controller itself. The implemented solution, inspired by biology, has been alluded to earlier [15], enabling the tuning of the desired force/displacement characteristics. However, these characteristics currently come at the cost of a sudden change in force magnitude while starting to converge and the lack of force feedback loop required for tasks such as haptic exploration.

A. Altering Fractal Impedance Profile for Force Homogeneity

The fractal attractor proposed in [15], [16] uses the conservation of energy principle to calculate the desired impedance for convergence, leading to a change of the gradient of energy at the inversion point that results in a sudden change in the exerted force. A solution to this issue may be provided by considering an agonist/antagonist control strategy, in which the two systems are impedance connected in parallel and the total produced effort (i.e., force) can be corrected by modulating the antagonist impedance, which alters the energy output through the port and smooths the force transition. However, the stability of the controllers can be retained only if this energy difference is corrected by modulating the antagonist impedance, which is the displacement associated with the force saturation, \( F_{\text{Max}} \) is the saturation force, \( b = (\tilde{x}_b - \tilde{x}_0)/S \) is the characteristic length of the sigmoidal function. \( S = 20 \) controls the saturation velocity ensuring that the force is at 99.9% of \( F_{\text{Max}} \) before reaching \( \tilde{x}_b \). The energy profile associated with this force profile is as follows:

\[
E_K = \begin{cases} 
0.5K_0\tilde{x}^2, & |\tilde{x}| < \tilde{x}_0 \\
F_{\text{Max}}|\tilde{x}| - F_{\text{Max}}\tilde{x}_0 + \left(K_0\tilde{x}_0^2/2\right) & |\tilde{x}| \geq \tilde{x}_0
\end{cases}
\]

If these profiles are used in the fractal impedance controller algorithm introduced in [15], they generate a non-smooth transition while switching from divergence to convergence. The force transition can be smoothed using the Algorithm 1. However, this algorithm introduces a discrepancy between

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**Fig. 3.** (a) The difference between the energy released in the environment force transition during inversion. As a consequence, an increase in the energy generated at the switching point by the two impedance elements are perfectly from the fractal impedance and the proposed method for obtaining smooth released into the environment emerges in the interval \((\tilde{x}_0, \tilde{x}_b)\), indicated in once the force saturates when \(|\tilde{x}| \) is greater than \( \tilde{x}_b \). (b) The forces/torques superimposed when using the proposed method.
the accumulated and the released energy (Figure 3a). The virtual antagonistic muscle is introduced to account for the energy discrepancy in the stability analysis. The Lyapunov proof is included in Appendix A, which updates the proof given in [15].

**Algorithm 1: Mono-dimensional Fractal Impedance Control**

**input:** Divergence/Convergence, $F_K(\bar{x})$, $E_K(\bar{\delta}_{\text{Max}})$, \( \bar{\delta}_{\text{Max}} \), \( \bar{x} \), $F_K(\bar{\delta}_{\text{Max}})$

**output:** \( h_c \)
1. if diverging from \( x_d \) then
2. \( h_c = F_K(\bar{x}) \)
3. else
4. if \( \bar{x} \leq x_0 \) then
5. \( h_c = F_{AA}(\bar{x}) = \frac{4E_K(\bar{\delta}_{\text{Max}})}{\bar{\delta}_{\text{Max}}} (\bar{x} - 0.5\bar{\delta}_{\text{Max}}) \)
6. else
7. \( h_c = F_{AA}(\bar{x}) = \frac{2E_K(\bar{\delta}_{\text{Max}})}{\bar{\delta}_{\text{Max}}} (\bar{x} - 0.5\bar{\delta}_{\text{Max}}) \)
8. end
9. end

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**B. Force Feedback**

A system interacting with an external entity does not only affect the environment but it is also affected by it. Therefore, the feed-forward dynamic interaction enabled by the impedance controller is not sufficient to guarantee the chosen behaviour during interaction. In fact, the environmental impedance will act as a parallel impedance to our controller modifying the resultant behaviour, which implies that we need to adjust \( \bar{x} \) to achieve the desired interaction force. An easy to visualise analogue is considering two springs pushing against each other, with one having a tunable stiffness. It is commonly known that the equilibrium point depends on their relative stiffness. Therefore, if we do not directly alter the exchanged force, we need to adjust the stiffness which also alters the equilibrium point.

An impedance controller interacting with an infinitely rigid system (i.e., non-deformable) produces the force at the interface predicted by the selected impedance model. However, the displacement (\( \bar{x} \)) required to achieve the same force will change when interacting with non-rigid systems, based on their relative stiffness. The parallel Force/Position control was proposed to solve this issue by adjusting the desired position based on a model of the interaction dynamics [19]. The major drawback of that approach was that being applied to a traditional impedance controller, an accurate model and a proper tuning of the impedance controller are essential for retaining the stability. However, the fractal impedance controller does not have such limitations, because the stability condition is embedded into the topology of controller attractor, cf. Fig. 2. This in turn implies that the availability of an accurate expectation of the environment will only enable a more efficient interaction. Thus, an online force feedback-based haptic exploration (Algorithm 2) can be deployed without introducing any concerns for the controller stability.

**Algorithm 2: Haptic Exploration**

**input:** \( F_d, K_0, \sigma, F(t-1), \bar{x}, x_0, x_0^b(t-1) \)

**output:** \( x_0^b(t) \)
1. \( \delta x_0 = \frac{F_d}{K_0} \)
2. \( \delta x_0^b = \sigma \delta x_0 \)
3. if \( F(t-1) = F_d(t) \) then
4. if \( |\bar{x}| \leq |x_d| \) then
5. \( x_0^b(t) = x_d + \delta x_0 \)
6. else
7. \( \Delta x = \frac{(F_d(t)-F_d(t-1))}{F_d(t)} \delta x_0^b \)
8. \( x_0^b(t) = x_0^b(t-1) + \Delta x \)
9. end
10. else
11. \( x_0^b(t) = x_0^b(t-1) \)
12. end

where: \( t \) is the discrete time variable,
\( F_d \) is the desired force,
\( x_0 \) is the displacement from the reference position
that is expected when making contact with the environment,
\( \sigma = 0.01 \) scaling factor for the force scanning resolution.

Lastly, it shall be noted that the proposed algorithm is made possible because within the fractal impedance controller the conservative field determined by the stiffness is the only source of energy. Therefore, the only interaction that can alter the topology generated by the controller stiffness is the coupling with an external non-infinite stiffness. On the other hand, the mass and damping component will affect only the path taken for converging to the desired behaviour.

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**III. EXPERIMENTAL DESIGN**

A simulator is a good approach for the preliminary evaluation of the proposed method because it allows direct control of the mechanical properties of the components involved without building a dedicated structure. This allows us to study how changes in properties of the external dynamics affect the controller performance and vice versa. The simulations are realised in Simulink (MathWorks, Inc). The solver is the ode4 with a constant time-step of 10 ms for continuous contact dynamics. The variable step solver ode23t has been used due to issues encountered in solving the model of the switching contact dynamics. The simulations were run using an Intel i7-7700HQ CPU with 16 GB of memory.

The simulation setup is described in Fig. 4, and the system dynamics simulated for 10 s. The parameters that have been kept unchanged across all the simulation are \( F_{\text{Max}} = 15 \text{ Nm}, \bar{x}_0 = 0.11 \text{ rad}, \bar{\delta}_0 = 0.10 \text{ rad} \) and \( I = 10 \text{ kg m}^2 \). The implemented hard-stop has no transition region for the dynamics and an undamped rebound. The experiments presented in this paper target the study of the influence of the environmental
stiffness changes on the controller performance and the evaluation of the effect of contact estimation error on the controller’s performance.

**Welded Parallel Connection To Spring-Damper Mechanism:** The simulation studies a system controlled by the proposed method "welded" to a spring-damper mechanism. The environmental parameters have been set to $K_{env} = 100 \text{ N m rad}^{-1}$ and $D_{env} = 189.7 \text{ N m s rad}^{-1}$. The values of $K_0$ chosen for this simulation are 0.1, 10, 100, and $1000 \text{ N m rad}^{-1}$. The strongest descriptors of the qualitative behaviour of the system are the relative stiffness and damping between the controller and the environment. The parameters selected for the experiments cover the different emergent behaviours.

**Controller Interaction with a Spring-Damper Mechanism:** The controller constant stiffness selected for these experiments is $K_0 = 100 \text{ N m rad}^{-1}$ and is equal to the $K_{env}$ used in the previous experiment. This simulation is subdivided as follows:

1) Effect of the change from welded to contact connection changes the system evolution.

2) Interaction with different values of environmental stiffness. The ($K_{env}$) evaluated are $50 \text{ N m rad}^{-1}$ and $500 \text{ N m rad}^{-1}$.

3) Performance changes introduced by different ($D_{env}$) values. The selected values are 0 and $63.2 \text{ N m s rad}^{-1}$, which is the critical damping for a system with $I = 10 \text{ kg m}^2$, and $K_{env} = 100 \text{ N m rad}^{-1}$.

During the first simulation, the inertial component starts in contact with the hard-stop, while it starts at 0.5 rad away for the other two simulations. $T_d$ for the last two experiments have been chosen to be $5 \text{ N}$, which is in the linear stiffness region ($\tilde{k} < \tilde{k}_0$) for the selected parameters.

**IV. Results**

The results for the Normalised Mean Square Error of the torque tracking error ($\tilde{T}$) for the simulations are reported in Fig. 6 and Fig. 7. The MSEs for the welded connection are always contained below $10^{-1}$ of the desired torque even when considering the transient period, and they drop below $10^{-4}$ in the last 5 s of the simulated trajectories. However, the introduction of the contact connection shows an increase in $\tilde{T}$ to about $10^{-1}$ of the desired torque even at the regime. This indicates that a unilateral connection to an external system is already a source of uncertainty that degrades the performance. The data reported in Fig. 7 further indicate that the errors increase even more when introducing the impact with the external environment, wherein some cases they can even reach two times the desired torque.

The time trajectories of the force and position tracking show a transient of about 0.5 s in the case of welded contact (Fig 7), which increases to about 1 s when introducing the contact dynamics (Fig 8). The time data analysis for the other experiments shows that despite the high impulsive force generated at the impact, the controller can retain contact in all the simulations, reported in Fig. 9 and Fig. 10. Furthermore, the data show that the torque error is always negative ($T < T_d$). $\tilde{T}$ is still reducing but at an extremely slow rate indicating that may be related to the choice of $\sigma$ in Algorithm 2.

**V. Discussion**

The results indicate that the proposed method can safely interact with external dynamics, and it can deal with the impulsive perturbation received when making contact. The controller passivity also enables to modify the controller parameters online without concerns for its stability.

The data also show that some trade-off needs to be made for obtaining robustness of interaction, particularly when tracking the desired forces. However, other methods are not exempt from similar trade-offs on the torque tracking accuracy when increasing interaction robustness. Differently from these methods, the proposed controller stability is not associated with the external environment but it is an intrinsic property of the controller. Therefore, it requires fewer assumptions on the environmental dynamics, and if they are violated it degrades the system accuracy but it does not lead to a catastrophic failure of the controller. This inherently safe behaviour is one of the key advantages of our proposed method for the control of real-world robotic systems interacting safely with people and environments.

The integration of Algorithms 1 and 2 into the architecture presented in Fig. 1 has shown that it is possible to reproduce behaviours similar to the one generated by agonist and antagonist muscles in biological systems. This architecture enables the online adaptation of the impedance behaviour without affecting the system stability, which is similar to what has been observed in human by previous studies [9], [11], [20], [21]. The ability to retain the stability during a wide range of unknown dynamic conditions is desirable for applications such as human-robot interaction (e.g., haptics, rehabilitation robots, and prosthetics), control of cable-driven systems where it may difficult to accurately model the transmission dynamics, and soft robotics. This framework
may also find application in modelling human motor control, where the possibility of superimposing multiple controllers may provide a platform to better understand motor synergies.

In conclusion, the proposed method has been proven feasible, and it shows a good level of performance when it is applied on a bilateral (welded) connection to the environment. The introduction of unilateral contact dynamics increases the force tracking error, however, it does not interfere with the ability of the controller to retain contact and stability of interaction. The residual tracking error seems to be related to the choice of the $\sigma$ parameter in Algorithm 2, which should be exposed and optimised by interaction. However, the data also show that this problem can be solved simply by setting $F_{\text{Max}} = T_d$. This also enables a
Fig. 7. The evolution of the torque error over time for different stiffness shows that the higher normalised MSE for $K_0 = 1$ and $T_d = 1$ is mainly related to a too wide search step implemented by Algorithm 2. It can also be seen that the torque error for $T_d = 20$ saturates at 5 N while the controller saturation torque is set at 15 N.

Fig. 8. The introduction of the contact dynamics renders the torque evolution smoother for $K_0 = 1$ and $T_d = 1$ and generally increases the convergence time for all the considered cases.

Fig. 9. After making contact the system never breaks it indicating the robustness of the controller which can deal with the impact dynamics without any significant issues. The residual error shows that the applied torque is less than the desired. A decreasing trend is still present in all case but with an extremely low rate of convergence.

Fig. 10. The interaction with an undamped environment shows similar post-contact behaviour of the damped interactions in Fig. 9. However, the removal of the damping introduces an initial oscillatory behaviour that replaces the torque spike present when making contacts in Fig. 9.

higher convergence speed to the desired torque. The passivity of the controller further implies that multiple controllers can be superimposed without interfering with the system stability. This provides a framework to develop a hierarchical architecture of semi-autonomous controllers that can be used to study human motor control and improve robots dynamic
interaction performances—a focus of our future work.

APPENDIX

A. Lyapunov’s Stability Analysis

The fractal impedance has a non-smooth piece-wise energy manifold with a time-invariant topology that scales with the controller gains by it does not change shape [15]. Let’s now consider the controller autonomous dynamics for a monodimensional system generated via Algorithm 1:

$$\begin{align*}
\dot{\Lambda} x + F_K(x) &= 0 \\
\dot{\Lambda} x + F_{AA}(x) &= 0
\end{align*}$$

$$V = \begin{cases} 
V_K = (\dot{x}^T \Lambda \dot{x})/2 + E_K(\dot{x}) \\
V_{AA} = (\dot{x}^T \Lambda \dot{x})/2 + E_{AA}(\dot{x}) + E_C 
\end{cases}$$

where $E_C$ is a constant of energy offset introduced in the switching conditions. Thus, $V$ time derivative is:

$$\begin{align*}
\dot{V}_K &= (\dot{\Lambda} x + F_K(\dot{x}))(\dot{x}) = 0 \\
\dot{V}_{AA} &= (\dot{\Lambda} x + F_{AA}(\dot{x}))(\dot{x}) = 0
\end{align*}$$

Therefore, the conditions for stability are respected in both the branches of the system. Nevertheless, being the system non-smooth to prove stability is needed to verify if $V$ is a Lipschitz function during the switching conditions. Being $V = 0$ at the switching conditions due to $x = 0$.

$$\begin{align*}
\lim_{\dot{x} \to 0} V_K &= E_K(\dot{x}_{\text{Max}}) \\
\lim_{\dot{x} \to 0} V_{AA} &= E_{AA}(\dot{x}_{\text{Max}}) + E_C \\
\lim_{\dot{x} \to 0} V_K &= 0 \\
\lim_{\dot{x} \to 0} V_{AA} &= E_{AA}(0) + E_C
\end{align*}$$

The continuity condition can be derived using the following system of equations:

$$E_C = E_K(\dot{x}_{\text{Max}}) - E_{AA}(\dot{x}_{\text{Max}})$$

$$E_C = -E_{AA}(0)$$

being:

$$E_{AA}(0) = \int_{\dot{x}_{\text{Max}}/2}^{\dot{x}_{\text{Max}}/2} F_{AA}(\dot{x}) d\dot{x} = -\int_{0}^{\dot{x}_{\text{Max}}/2} F_{AA}(\dot{x}) d\dot{x}$$

$$E_{AA}(\dot{x}_{\text{Max}}) = (E_K(\dot{x}_{\text{Max}}) - \Delta E_{AA|\dot{x}_{\text{Max}}})/2$$

and given that the energy contribution of antagonist muscle ($\Delta E_{AA|\dot{x}_{\text{Max}}}$) always opposes to the motion:

$$E_C = -E_{AA}(0) = (E_K(\dot{x}_{\text{Max}}) - \Delta E_{AA|\dot{x}_{\text{Max}}})/2$$

which implies:

$$\begin{align*}
V_{AA}(0) &= 0 \\
V_{AA}(\dot{x}_{\text{Max}}) &= E_K(\dot{x}_{\text{Max}})
\end{align*}$$

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