ASTEROSEISMIC-BASED ESTIMATION OF THE SURFACE GRAVITY FOR THE LAMOST GIANT STARS

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ABSTRACT

Asteroseismology is one of the most accurate approaches to estimate the surface gravity of a star. However, most of the data from the current spectroscopic surveys do not have asteroseismic measurements, which is very expensive and time consuming. In order to improve the spectroscopic surface gravity estimates for a large amount of survey data with the help of the small subset of the data with seismic measurements, we set up a support vector regression (SVR) model for the estimation of the surface gravity supervised by 1374 Large Sky Area Multi-object Fiber Spectroscopic Telescope (LAMOST) giant stars with Kepler seismic surface gravity. The new approach can reduce the uncertainty of the estimates down to about 0.1 dex, which is better than the LAMOST pipeline by at least a factor of 2, for the spectra with signal-to-noise ratio higher than 20. Compared with the log g estimated from the LAMOST pipeline, the revised log g values provide a significantly improved match to the expected distribution of red clump and red giant branch stars from stellar isochrones. Moreover, even the red bump stars, which extend to only about 0.1 dex in log g, can be discriminated from the new estimated surface gravity. The method is then applied to about 350,000 LAMOST metal-rich giant stars to provide improved surface gravity estimates. In general, the uncertainty of the distance estimate based on the SVR surface gravity can be reduced to about 12% for the LAMOST data.

Key words: asteroseismology – methods: data analysis – methods: statistical – stars: fundamental parameters

1. INTRODUCTION

The surface gravity of a star is an important stellar astrophysical parameter in the sense that it is able to measure the radius of a star given the stellar mass. Together with the effective temperature and metallicity, a star can be pinned down in the Hertzsprung–Russell diagram with the surface gravity. This will be very helpful to learn the evolution status of the star, as well as its distance. Therefore, an accurate estimation of the surface gravity is critical in the study of either stars or stellar systems.

Although multiband photometry may help to discriminate giant from dwarf stars according to some surface-gravity-sensitive features (Lenz et al. 1998; Majewski et al. 2000; Yanny et al. 2000), spectroscopic data can reveal more detailed features to quantify the surface gravity. First, the prominent Mg b+Mg H feature observed in low-resolution spectra is used not only to identify giant stars (Liu et al. 2014; Xue et al. 2014), but also to measure their surface gravity (Morrison et al. 2003; Lee et al. 2008). Second, the other features, e.g., Balmer lines (Wilhelm et al. 1999), Ca ii, K, and H lines (Lee et al. 2008), etc., can also be useful to the determination of the surface gravity. Moreover, some algorithms determine the surface gravity together with the effective temperature and metallicity simultaneously, by comparing the full spectra with the spectral library (e.g., Lee et al. 2008; Wu et al. 2011b). In addition, the supervised machine learning approaches, e.g., artificial neural networks, support vector machine (SVM), etc., have also been used to derive the surface gravity based on the training spectra with known surface gravity values as the targets (Re Fiorentin et al. 2006; Liu et al. 2012). The typical accuracy of the surface gravity estimates for low-resolution spectra, e.g., the Sloan Digital Sky Survey (SDSS; Ahn et al. 2014) or the Large Sky Area Multi-object Fiber Spectroscopic Telescope (LAMOST; Cui et al. 2012), is about 0.2–0.4 dex (Wilhelm et al. 1999; Re Fiorentin et al. 2006; Lee et al. 2008; Wu et al. 2014).

Asteroseismology is a powerful tool to derive the fundamental parameters, e.g., stellar mass, radius, and log g, for a star (see Brown & Gilliland 1994; Chaplin & Miglio 2013). Thanks to the Kepler (Borucki et al. 2010) mission, the solar-like oscillations for tens of thousands of stars are able to be measured. The surface gravity can be estimated from the oscillations with accuracy of 0.02–0.05 dex (Morel & Miglio 2012; Creevey et al. 2013). This performance is much better than the non-seismic methods from even the high-resolution spectra. Indeed, Epstein (2014b) has shown that the Kepler-measured seismic log g is more accurate than those from the high-resolution infrared APOGEE (Majewski et al. 2010) spectra by a factor of a few.

However, compared to the huge amount of spectra from many large spectroscopic survey projects, the number of stars with asteroseismic measurement is still very limited. Therefore, it is crucial to examine how the surface gravity of all the spectroscopic survey data can be improved with the existing seismic data, which only occupies a small fraction of the full samples. In this paper, we give more accurate log g estimates for the LAMOST data with the help of a small subset of the spectra with Kepler seismic log g.

LAMOST, also known as the Guoshoujing Telescope, is a new type of 5° wide field telescope with a large aperture of 4 m. It assembles 4000 fibers on its large focal plane and can simultaneously observe a similar number of low-resolution ($R \sim 1800$) spectra covering the wavelength from 380 to 900 nm (Cui et al. 2012; Zhao et al. 2012). As its main scientific goal, it will observe a few millions of stellar spectra with limiting magnitude down to $r \sim 18$ mag for diverse
studies of the Milky Way (Deng et al. 2012). It has also sampled the Kepler field with the “LAMOST-Kepler project” (De Cat et al. 2014), in which a few thousand spectra with Kepler seismic data (Huber et al. 2014) are included. This small subset provides perfect calibrators to improve the estimation of log g for the LAMOST spectra.

In this work, we develop a support vector regression (hereafter SVR) model for the determination of the surface gravity for the LAMOST giant stars supervised by the data with Kepler seismic log g. The paper is organized as follows. In Section 2, we give a detailed introduction to SVR. Then, we specifically set up an SVR model to estimate log g for LAMOST data in Section 3. The performance of the determination is also assessed in this session. Some discussions, including the systematics from the seismic log g, the influences in various evolution phases of the stars, the metallicity effect, the comparison with other similar works, and the benefits and limits of this technique, are raised in Section 4. Finally, a brief conclusion is drawn in the final section.

2. SUPPORT VECTOR REGRESSION

SVM is a well-known supervised machine learning algorithm mostly in the application of classification and nonlinear regression (Cortes & Vapnik 1995; Burges 1998; Deng et al. 2012). SVR (Drucker et al. 1996), as an extension of the SVM, is a regression method by transforming the data, via a kernel function, from the nonlinear physical space into a high-dimensional inner-product space, in which a linear model to the data can be fitted.

We refer the reader to Smola & Schölkopf (2004) for a complete description of SVR. We only give an outline of the approach. Assume that \{(x_1, y_1), (x_2, y_2), \ldots, (x_n, y_n)\} are the training data, where \(x_i\) is the input vector in d dimensions and \(y_i\) is the corresponding known output. Because the relationship between \(x\) and \(y\) is highly nonlinear, the SVR is to find a map, \(\Phi\), mapping the real input space to a higher-dimensional feature space, in which the nonlinear regression problem can be converted into a linear problem. For this purpose, the SVR constructs a form such as

\[
f(x) = \sum_{i} \left( \alpha_i - \alpha_i^* \right) \Phi(x_i) + b, \tag{1}
\]

where \(\langle \cdot, \cdot \rangle\) is the inner product and \(\alpha_i, \alpha_i^*,\) and \(b\) are parameters to be solved. Practically, \(\Phi\) is not explicitly given, but uses a kernel function, \(K(x, x') \equiv \langle \Phi(x), \Phi(x') \rangle\), instead. Among lots of choices of the kernels, the radial-based kernel, which has the form of \(\exp(-\gamma ||x - x'||^2)\), is often used. Mathematically, it can be proved that \(f\) is linear in the inner-product space. The solution of Equation (1) can be derived from a convex optimization problem:

minimize \(\frac{1}{2} \|w\|^2 + C \sum_{i=1}^{n} (\xi_i + \xi_i^*)\)

subject to \(y_i - \langle w, \Phi(x_i) \rangle - b \leq \epsilon + \xi_i\)

\(\langle w, \Phi(x_i) \rangle + b - y_i \leq \epsilon + \xi_i^*\) \tag{2}

\(\xi_i, \xi_i^* \geq 0\)

where \(w = \sum_{i=1}^{n} (\alpha_i - \alpha_i^*) \Phi(x_i), C > 0\) is the cost parameter to determine the trade-off between the flatness of \(f\) and the amount up to which deviations larger than \(\epsilon\) are tolerated, and \(\xi_i\) and \(\xi_i^*\) are slack variables. Figure 1 demonstrates how the SVR works in the linear case.

Chang & Lin (2011) provide a multi-programming language package, LIBSVM,\(^6\) to solve the SVR model based on Equations (1) and (2), as well as other SVM models. The process of finding the optimized solution of the SVR model contains two steps. The first step is to determine the parameters \(C, \epsilon, \) and \(\gamma\) from \(n\)-fold cross-validations. In this step, the software randomly divides the training data set into \(n\) groups with equal size and predicts the dependent values for each group using the SVR model trained by the remaining \(n-1\) groups of data. The best choices of \(C, \epsilon,\) and \(\gamma\) are those that give the best cross-validation accuracy of the regression. The second step is to find the optimal solution of \(\alpha_i, \alpha_i^*, \xi_i, \xi_i^*\), and \(b\) in Equation (2) for the whole training data set using the best choices of \(C, \epsilon,\) and \(\gamma\). Then, the derived SVR model, Equation (1), can be used to predict the corresponding dependent variable for given input data. A typical application of the SVR is also found in Liu et al. (2012).

3. ESTIMATE LOG G FOR LAMOST SPECTRA

3.1. The Training and Test Data Set

In order to establish an SVR model for the log g determination based on the seismic estimates, we first select a proper training data set. Huber et al. (2014) released \(\sim 200,000\) stars with stellar parameters in the Kepler field, among which 15,686 stars have surface gravity estimated from asteroseismology (hereafter, we call it the Huber catalog). We use the parameters listed in Table 4 of Huber et al. (2014), which is directly compiled from literature and not fitted to the model isochrones. We cross-identify these stars with the LAMOST DR2 data and obtain 3335 common stars with the signal-to-noise ratio (S/N) at g band higher than 10 in the

\(^6\)http://www.csie.ntu.edu.tw/~cjlin/libsvm/
is the frequency of maximum power and the Å·

Equation rescaling:

log
to be recalibrated with LAMOST

Therefore, the initial seismic log and

empirical stellar library ELODIE as a reference

estimated in the pipeline using the software (Wu et al. 2011a, 2011b, 2014)

The scaling relation of the seismic log

g, as shown in Equation (3), depends on $T_{\text{eff}}$:

$$
\frac{g}{g_{\odot}} \simeq \left( \frac{\nu_{\text{max}}}{\nu_{\text{max,\odot}}} \right) \left( \frac{T_{\text{eff}}}{T_{\text{eff,\odot}}} \right)^{0.5},
$$

where $\nu_{\text{max}}$ is the frequency of maximum power and the quantities with $\odot$ stand for the solar parameters (Chaplin & Miglio 2013). The effective temperature used to derive the seismic log in the Huber catalog may not be consistent with the LAMOST $T_{\text{eff}}$. Indeed, Figure 2 shows that the LAMOST $T_{\text{eff}}$ is smaller than those in the Huber catalog by about 200 K. Therefore, the initial seismic log $g$ in the Huber catalog needs to be recalibrated with LAMOST $T_{\text{eff}}$. Without providing the frequencies of the seismic oscillation in the Huber catalog, we can recalculate the seismic log $g$ by applying the following rescaling:

$$
g_{\text{ast,corr}} = g_{\text{ast,Huber}} \left( \frac{T_{\text{eff,LM}}}{T_{\text{eff,Huber}}} \right)^{0.5},
$$

where $T_{\text{eff,LM}}$ is the LAMOST-derived effective temperature and $T_{\text{eff,Huber}}$ and $g_{\text{ast,Huber}}$ are the effective temperature and the seismic surface gravity provided by the Huber catalog, respectively. In order to keep self-consistence of $T_{\text{eff}}$ in the Huber catalog, we only use the objects with Pinsonneault et al. (2012) $T_{\text{eff}}$ or whose $T_{\text{eff}}$ is calibrated with Pinsonneault et al. (2012) in the Huber catalog. Consequently, a very small fraction of stars, which are from the references 6, 13, and 14 and hence may not explicitly calibrate to Pinsonneault et al.

We use the S/N at $g$ band because most of the spectral lines sensitive to log $g$ are located in this range of wavelength (Liu et al. 2014).

scales. The stellar parameters of these LAMOST spectra are estimated in the pipeline using the software ULySS, with the empirical stellar library ELODIE as a reference (Wu et al. 2011a, 2011b, 2014).

The scaling relation of the seismic log $g$, to be recalibrated with LAMOST $T_{\text{eff,LM}}$, is expressed as

Figure 2: Difference between the LAMOST $T_{\text{eff}}$ and the $T_{\text{eff}}$ in the Huber catalog. The x-axis is the LAMOST $T_{\text{eff}}$, and y-axis is the difference of the $T_{\text{eff}}$ between LAMOST and the Huber catalog. The black dots stand for the individual stars in the training data set, and the red filled circles with error bars indicate the medians and dispersions of the differences at various $T_{\text{eff}}$ bins.

Figure 3: Difference between the initial log $g$ from the Huber catalog and the recalibrated one using LAMOST $T_{\text{eff,LM}}$. The x-axis is the recalibrated log $g$, while the y-axis is the difference. The black dots stand for the stars in the training data set, and the red filled circles with error bars are the medians and dispersions of the differences at various log $g_{\text{ast,corr}}$ bins.
model. These line indices are more robust to the noise than the full spectrum.

In general, if the line indices vary with log $g$ in the same way as with $T_{\text{eff}}$, then it is not easy to distinguish whether the change of the line indices is caused by the change of log $g$ or $T_{\text{eff}}$. This is the so-called degeneracy between log $g$ and $T_{\text{eff}}$. For instance, H$_{\alpha}$, H$_{\beta}$, and TiO show similar trends of variation when either log $g$ or $T_{\text{eff}}$ changes (see Figures 4 and 5). However, not all of the 23 Lick line indices are affected by the degeneracy. The lines such as Mg$_{1}$, Mg$_{2}$, Mg$_{b}$, Fe5335, Fe5782, etc., vary with log $g$ in a different way with $T_{\text{eff}}$ (also see Figures 4 and 5). Therefore, these lines are more helpful to break the degeneracy and allow us to estimate log $g$. Figure 6 also shows that the variations of [Fe/H] in the line indices are quite different with log $g$, meaning that there is relatively little degeneracy between [Fe/H] and log $g$.

Although the SVR model can only deal with a one-dimensional dependent variable, it may not produce systematically biased log $g$ estimates related to either $T_{\text{eff}}$ or [Fe/H], because the training data set covers the same ranges of the metallicity and effective temperature as the test data set and the full LAMOST sample. More investigations will be discussed in Section 3.2.

It is also worthwhile to notice that although the asteroseismic log $g_{\text{ast}}$ is used as the known dependent variable in the training data set, it does not mean that the seismic log $g$ is the true value for a star. It is also affected by some systematics, as mentioned later in Section 4.1. However, compared to the relatively larger uncertainty of the spectroscopic log $g$ estimates, the systematic bias in the seismic log $g$ is quite small and can be negligible. Moreover, the motivation of this work is not to find the true log $g$ for the spectra, but to find the better log $g$ estimates than the other spectroscopic methods. Since the seismic log $g$ is so far the best choice, the goal of this work is to calibrate the log $g$ estimated from the low-resolution spectra to the best one, i.e., the seismic log $g$.

Note that the LAMOST-pipeline-derived log $g_{\text{LM}}$ is only used in the initial data selection; it plays no role in the SVR model. In other words, the SVR-predicted log $g_{\text{SVR}}$ is independent of log $g_{\text{LM}}$.

### 3.2. Performance

In this section we use the test data set with 1352 stars, which do not appear in the training data set but have seismic log $g$ and similar ranges of $T_{\text{eff}}$ and [Fe/H] to the training data set, to investigate the performance. The recalibrated seismic log $g_{\text{ast}}$ is used as the standard value to be compared with in the whole performance assessment.

An intuitive assessment of the performance of the SVR model is to compare the SVR log $g$ (denoted as log $g_{\text{SVR}}$) with other estimates in the $T_{\text{eff}}$–log $g$ diagram. Figure 7 shows three $T_{\text{eff}}$–log $g$ diagrams for the test data set with $S/N(g) > 20$; the $y$-axes are log $g_{\text{LM}}$, log $g_{\text{ast}}$, and derived log $g_{\text{SVR}}$ from panels (a) to (c), respectively. The $x$-axes, log $T_{\text{eff,LM}}$, in the three panels are all from the LAMOST pipeline. The red dashed lines show the isochrones (Marigo et al. 2008) with [Fe/H] = −0.2 dex at the age of 1, 5, and 10 Gyr, from top to bottom.

First, the largest difference between log $g_{\text{LM}}$ and the other two is that for the red giant branch (RGB) stars, which are located below the isochrones for log $g_{\text{LM}}$ (panel (a)). This can also be clearly seen in Figure 8, in which the difference of the log $g_{\text{SVR}}$ and log $g_{\text{LM}}$ is below the zero point by 0.5 dex for stars with log $g_{\text{SVR}} < 2$ dex. Although it cannot be used to justify whether or not the LAMOST result is correct, the discrepancy between log $g_{\text{LM}}$ and the isochrone does bring significant systematic bias when one determines the distance by comparing log $g_{\text{LM}}$ and $T_{\text{eff,LM}}$ with the synthetic isochrones. The seismic (panel (b)) and SVR (panel (c)) log $g$, on the other hand, are consistent with the isochrones for the RGB stars.

Second, the most prominent feature in the $T_{\text{eff}}$–log $g$ diagrams is the red clump/bump stars which concentrate at around log $g$ ~ 2.5 dex and log $T_{\text{eff}}$ ~ 3.68. Compared with the seismic log $g$, the LAMOST-derived red clump stars (panel (a)) show an obviously tilted shape, which is probably an artificial effect due to the incompleteness and sparseness of the stellar library used in the current LAMOST pipeline. As the most accurate measurement of log $g$, the seismic log $g$ shows the clear red bump located at 0.1–0.3 dex below the more concentrated and horizontally elongated red clump stars (log $g$ ~ 2.4 dex, 3.64 < log $T_{\text{eff}}$ < 3.7) in panel (b). Encouragingly, the SVR log $g$ shows similar features in panel (c): (1) the red clump is more concentrated than the LAMOST log $g$ and also shows a slightly elongated shape at 3.65 < log $T_{\text{eff}}$ < 3.7; (2) the red bump stars can be barely discriminated just 0.3 dex below the red clump at log $T_{\text{eff}}$ ~ 3.65, although the dispersion is larger than the seismic log $g$.

Figure 8 shows the difference between the SVR and LAMOST log $g$. For the stars with log $g_{\text{SVR}} > 2.5$ dex, log $g_{\text{SVR}}$ is slightly smaller than log $g_{\text{LM}}$ by about 0.1 dex. For those with log $g_{\text{SVR}} < 2.5$ dex, log $g_{\text{SVR}}$ is significantly smaller than log $g_{\text{LM}}$ by ~0.5 dex. This means that the LAMOST-provided log $g$ may overestimate the log $g$ for the upper part of the RGB stars.

Figure 9 demonstrates the difference of the SVR with the seismic log $g$ as a function of the S/N at g band of the corresponding LAMOST spectra for the test data set. The two thin red lines in Figure 9 indicate the 1σ dispersion of the difference, which are flat at about ±0.1 dex when S/N(g) > 20. Although this uncertainty is still larger than the seismic measurement, it is significantly better than any other non-seismic estimation for the low-resolution spectra by a factor of 2–4. This explains why we can marginally distinguish the bump stars from the $T_{\text{eff}}$–log $g$ diagram with SVR log $g$ in panel (c) of Figure 7.

Figure 10 shows the performance of the SVR log $g$ compared with the corresponding seismic log $g$ using the test data set with S/N(g) > 20. First, the comparisons between the residual log $g$ (defined as log $g_{\text{SVR}}$–log $g_{\text{ast}}$) do not show any strong correlation with the effective temperature, as shown in panels (a). Second, it shows very weak anticorrelation with [Fe/H], i.e., the SVR log $g$ is very slightly overestimated for stars with [Fe/H] ~ −0.6 dex and underestimated for those with [Fe/H] ~ +0.2 dex. This systematic bias is below 0.05 dex, within the dispersion of the residual of log $g_{\text{SVR}}$. Third, in panel (c), for stars with log $g_{\text{ast}} > 3$ dex, the SVR log $g$ is underestimated by ~0.1 dex. Then the residual of log $g_{\text{SVR}}$ changes from negative to positive when log $g_{\text{ast}}$ changes from 3 to 2.25 dex. Considering that the dispersion of the residual in this range is slightly larger than 0.1 dex, this systematics is not

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8 Red clump stars are stars in the evolution phase of helium core burning; bump stars are the phase of first ascent RGB stars in which a slight drop in the luminosities occurs when the extremely thin hydrogen shell is crossing to the discontinuous region (Cassisi & Salaris 1997).
Figure 4. Correlations between log \( g \) and the 23 Lick indices for the training data set. The \( x \)- and \( y \)-axes are two different Lick indices, and the color codes give the
corrected seismic surface gravity.
Figure 5. Correlations between $T_{\text{eff}}$ and the 23 Lick indices for the training data set. The $x$- and $y$-axes are two different Lick indices, and the color codes give the effective temperature from the LAMOST pipeline.
Figure 6. Correlations between $[\text{Fe}/\text{H}]$ and the 23 Lick indices for the training data set. The $x$- and $y$-axes are two different Lick indices, and the color codes give the metallicity from the LAMOST pipeline.
significant, although it is not negligible. For those $\log g_{\text{ast}} < 2.25$ dex, a slight overestimation of less than 0.05 dex in $\log g_{\text{SVR}}$ is found. This inverse S-shape in the residual $\log g_{\text{SVR}}$ versus $\log g_{\text{ast}}$ is further discussed in Section 4.2. Finally, the distribution of the residual gives the overall uncertainty of the measurement in panel (d). The standard deviation for the residual is 0.16 dex. We also fit the distribution of the residual with a Gaussian to give an alternative estimation of the dispersion. The best-fit Gaussian (the red line) is centered at 0, meaning that there is no overall systematic bias in the SVR estimation, and $\sigma$ is 0.11 dex.

3.3. Apply to LAMOST Data

We apply the SVR $\log g$ estimator to 356,932 selected LAMOST DR2 stars with $\log g_{\text{LM}} < 4$ dex, $[\text{Fe/H}]_{\text{LM}} > -0.6$ dex, and reliably measured equivalent widths for all 23 line indices. The final result is shown in panel (a) of Figure 11. As a comparison, panel (b) shows a similar plot to the LAMOST-derived $\log g$. Compared with the theoretical isochrones, the underestimation in the LAMOST $\log g$ of the RGB stars has been corrected in the results of this work, and the shape around the red clump stars now seems normal. However, a small fraction of stars with $\log T_{\text{eff}} > 3.72$ are significantly underestimated in $\log g$ because of the poor quality of the corresponding spectra for these stars.

4. DISCUSSIONS

4.1. The Systematic Bias in Seismic Parameter Determinations

The SVR $\log g$ is automatically calibrated to the seismic $\log g$, since it uses the latter as the standard value in the training data set. This also means that all systematics that occur in seismic $\log g$ will also come into SVR $\log g$. Therefore, it is important that the users, particularly those who are not working in asteroseismology, of the SVR $\log g$ should be aware of the performance of the seismic scaling relations. Here we just briefly review a few of them related to...
The effective temperature $T_{\text{eff}}$ for the test data set with S/N and bars in the three panels indicate the medians and dispersions at various positions. Panel in this panel is the best-fit Gaussian, with parameters of offset = 0 and $\sigma = 0.11$ dex, to the residual. The standard deviation of the residual is 0.16 dex.

According to Equation (3), the accuracy of the surface gravity depends on a few factors: the frequency of maximum power $\nu_{\text{max}}$, the effective temperature $T_{\text{eff}}$, and the corresponding solar parameters. Gai et al. (2011) investigated the grid-based method to derive stellar properties, including log $g$, from seismic parameters combined with effective temperature and metallicity. They found that the uncertainty (in terms of FWHM of the distribution of the fractional deviation of the true value) is smaller for stars with large log $g$ than for those with small log $g$. In all cases, the uncertainty is within 5% of the true log $g$. Huber et al. (2012) combined the asteroseismology, interferometry, and photometry of the stars and found that the uncertainties of the seismic scaling relations are in agreement with other measurements, and the uncertainties do not depend on the evolution stage of the stars. However, Hekker et al. (2013) inferred that the seismic parameter determinations give small systematic bias in log $g$ for both red clump and RGB stars, although the extent of the systematics is within 0.01 dex. More investigations about the various evolution phases of stars are given in Section 4.2.

All these systematic biases do affect the SVR estimates for the LAMOST data, since the SVR treats the seismic log $g$ as the standard. Therefore, the users who intend to apply the log $g_{\text{SVR}}$ in any study of the structure and evolution of the Milky Way should very carefully validate whether these systematic biases affect their results.

It is also worthwhile to note that the limit of the techniques and observations in asteroseismology may bias the sampling of the giant stars at different log $g$. For the giant stars with larger log $g$, because their oscillation amplitude is very small (Huber et al. 2011) and thus hard to detect, many of these kinds of stars in the Kepler field lack asteroseismic log $g$. On the other hand, the giant stars with smaller log $g$ are also undersampled because their oscillation frequency is too low and cannot be reliably measured during the 4 yr observations with Kepler. Therefore, the training data set lacks data at both ends of the distribution of the log $g_{\text{est}}$. This may lead to some systematics in the SVR method because of the imbalance of the training data set. Fortunately, it seems that the training data set contains sufficient stars with either very small or very large log $g_{\text{est}}$ and the systematic bias shown in panel (c) of Figure 10 is acceptable, compared to the uncertainty of $\sim$0.1 dex.

### 4.2. Effect of Evolution Phases

Pinsonneault et al. (2014) found that the spectroscopic and seismic log $g$ are systematically different for the giant stars in different evolution stages, e.g., the primary red clump stars,
secondary red clump stars, and RGB stars. Although the training data set of the SVR model uses seismic log g, the input data are based on the spectra. Therefore, it may also have a similar systematic bias to that shown in Figure 3 of Pinsonneault et al. (2014). We then tag the primary and secondary red clump stars and RGB stars in the test data set by cross-identifying it with the data from Stello et al. (2013), in which the evolution phases are distinguished by the period spacings of the dipole mode. Figure 12 shows that log \( g_{SVR} \) is about 0.05 dex lower than log \( g \) for the RGB stars. Although almost no overall systematics is found for primary red clump stars, a few of them are overestimated by about 0.2 dex (see the left side of Figure 12). For the secondary red clump stars, the median residual slightly shifts to −0.03 dex. This can explain why in panel (c) of Figure 10 the SVR log g is systematically underestimated for stars with log \( g \) > 3 dex, which are mostly RGB stars, and then slightly overestimated for log \( g \) < 2.25 dex. Moreover, the dispersion of the residual between log \( g_{SVR} \) and log \( g \) is larger in RGB stars than in red clump stars. It seems that the effect of evolution phases in LAMOST is different from that in the APOGEE data (Pinsonneault et al. 2014). In future works, more investigations will be necessary to address the reason why the different evolution stages show different biases in log g estimates and to cross-calibrate the parameters between LAMOST and APOGEE data.

### 4.3. Metallicity

Currently, the seismic log g is limited to the metal-rich stars. This is because the empirical scaling relation used in the asteroseismology measurement is based on the solar-type stars. Epstein et al. (2014a) found that the seismic mass estimation for the halo and thick-disk stars is significantly higher than the expectations. Although the stellar radius estimation is more precise than the stellar mass (Gai et al. 2011), it may also be affected by the same systematic bias. Therefore, we only apply the seismic-trained SVR model to the metal-rich giant stars ([Fe/H] > −0.6 dex) to avoid the probably systematic shift for the metal-poor stars.

It is also worthwhile to compare the metallicity distribution functions (MDFs) of the training data set and the selected LAMOST data to ensure that the training data set covers the entire range of the metallicity of the LAMOST data. Figure 13 shows the two MDFs (the gray and red lines stand for the MDF of the training data set and the LAMOST data, respectively). Because both samples are cut at −0.6 dex, the two MDFs are truncated at this value. Although the peaks of the two distributions are different by about 0.2 dex, they approximately cover the same range of metallicity, except a very small fraction of data at about 0.4 dex. Therefore, the scaling relation of the seismology used in the surface gravity estimation for the training data set is also suitable for the selected LAMOST data.

Moreover, panel (b) of Figure 10 shows that log \( g_{SVR} \) does not strongly correlate with metallicity. Therefore, the slight difference of the MDFs shown in Figure 13 would not lead to significant systematics in the derived log g for the LAMOST data.

#### 4.4. Comparison with Other Works

Mészáros et al. (2013) and Holtzman et al. (2015) calibrated the surface gravity of the APOGEE (Ahn et al. 2014) data to seismic values with simple functions. Compared to the technique employed in this work, their methods are direct and simple. However, the measurement errors in their methods are contributed twice from two different processes: one is from the estimation of the initial log g based on a synthetic library, and the other is from the calibration after log g estimation. Therefore, the uncertainty of the calibrated log g may be intrinsically larger. In our method, the seismic log g is directly used as the standard values in the training process, and therefore the measurement error is only produced once during the determination of the log g. The derived log g from the SVR model is naturally calibrated with the seismic log g. In other words, the SVR model merges the two steps of determination and calibration of log g into one single step and hence avoids additional error contribution.
4.5. Degeneracies between \( \log g, T_{\text{eff}}, \) and \([\text{Fe/H}]\)

Figures 4–6 show that the stellar parameters, \( \log g, T_{\text{eff}}, \) and \([\text{Fe/H}]\), are not precisely orthogonal in the spectral lines. In some of the lines, the stellar parameters even change toward similar directions, producing some extents of degeneracies. It is quite difficult to completely break the degeneracies in a stellar parameterization technique, particularly in an algorithm like SVR, which can only determine one parameter at a time. Indeed, Figure 10 does show that the residuals of \( g_{\text{SVR}} \) bias from zero by at most \( \sim 0.05 \) dex in \( T_{\text{eff}} \) and \([\text{Fe/H}]\). However, considering that the \( g_{\text{SVR}} \) estimated in this work will be mainly used in the large sample statistics with tens or even hundreds of thousands of stars in the Galaxy, these weak biases may not significantly affect the results.

It is also noted that the SVR \( \log g \) may also change the estimation of \( T_{\text{eff}} \) and \([\text{Fe/H}]\). Figures 4–6 show that some spectral lines are sensitive to all three parameters. This means that when we estimate \( T_{\text{eff}} \) and \([\text{Fe/H}]\) with the adopted SVR \( \log g \) values, the derived \( T_{\text{eff}} \) and \([\text{Fe/H}]\) may be quite different from the current values from the LAMOST pipeline. The difference can be quantified by reestimating the \( T_{\text{eff}} \) and \([\text{Fe/H}]\) in the LAMOST pipeline with the fixed SVR \( \log g \) value. This, however, is beyond the scope of this paper and should be investigated in future works.

4.6. Benefits from Accurate \( \log g \)

We can significantly improve the accuracy of the distance estimation from accurate \( \log g \) estimates. Since the stellar luminosity follows \( L \propto R^2 \) and surface gravity follows \( g \propto R^{-2} \), we have \( L \propto g^{-1} \). Consequently, the absolute magnitude \( M \) is proportional to \( \log L \sim 2.5 \log g \). This means that when the uncertainty of \( \log g \) is 0.1 dex, the uncertainty of the absolute magnitude turns out to be 0.25 mag, which is equivalent with about 12% in distance.\(^{10}\) This is a factor of \( \sim 2 \) better than the accuracy of distance derived from the non-seismic-based spectroscopic \( \log g \) (Carlin et al. 2015).

4.7. The Dwarf Stars

The known \textit{Kepler} seismic \( \log g \) are mostly for the giant stars (Huber et al. 2014). Hence, we lack dwarf star samples as the training data set. As a consequence, we only apply the method to giant stars and do not expand it to dwarf stars. The LAMOST \( \log g \) is sufficiently accurate for the separation of the giant and dwarf stars. Therefore, we use it to select the giant stars first and let the seismic-trained SVR model predict more accurate \( \log g \) for the selected giant stars. In the future, the coming \textit{PLATO} mission may provide another tens of thousands of asteroseismic measurements over the entire Hertzsprung–Russell diagram (Rauer et al. 2014). This will help to enrich the dwarf training data set and expand this work to the dwarf stars.

5. CONCLUSIONS

Although we use the LAMOST spectra as the training data set, it does not limit the application of the SVR model only to the LAMOST data. In general, given other spectroscopic survey data without seismic measurement, we can first calibrate the equivalent widths of the line indices to align with LAMOST and then apply the model to the new data. Indeed, we test it using a set of MMT/Hectospec-observed giant stars, in which more than 100 common objects with LAMOST are found. The accuracy of the \( \log g \) estimates for these samples is roughly at the same level as in this work (more details will be given in C. Liu et al. 2015, in preparation).

In summary, although not all LAMOST data have asteroseismic observations, we can use a small subset with the \textit{Kepler} seismic \( \log g \) as the training data set to estimate \( \log g \) for other LAMOST data with an SVR model. The approach can reach to an accuracy as high as 0.1 dex when the S/N of the spectra is higher than 20. This improves the current \( \log g \) estimated from the LAMOST pipeline by at least a factor of 2. This significant improvement will be very useful in the following studies: (1) it allows us to better estimate the distance of the giant stars with accuracy of about 12%, and (2) it enables us to separate the primary and secondary red clump stars from \( \log g \), providing good samples to trace the stellar populations with different ages.

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\(^{10}\) Note that the accuracy of the distance does not take into account the uncertainties contributed by photometries, e.g., the coarse dereddening, less accurate magnitude, etc.
