Tunable 3D/2D magnetism in the \((\text{MnBi}_2\text{Te}_4)(\text{Bi}_2\text{Te}_3)_m\)
topological insulators family

Ilya I. Klimovskikh\(^1\), Mikhail M. Otrokov\(^{2,3}\), Dmitry Estyunin\(^3\), Sergey V. Eremeev\(^{1,4,5}\), Sergey O. Filinov\(^1\), Alexandre Koroleva\(^1\), Eugene Shevchenko\(^1\), Vladimir Voroshnin\(^6\), Artem G. Rybkin\(^1\), Igor P. Rusinov\(^1,5\), Maria Blanco-Rey\(^7,8\), Martin Hoffmann\(^9\), Ziya S. Aliev\(^{10,11}\), Mahammad B. Babanly\(^{12,13}\), Imamaddin R. Amiraslanov\(^{11,13}\), Nadir A. Abdullayev\(^{11,13}\), Vladimir N. Zverev\(^{14}\), Akio Kimura\(^{15}\), Oleg E. Tereshchenko\(^{11,16,17}\), Konstantin A. Kokh\(^{1,17,18}\), Luca Petaccia\(^{19}\), Giovanni Di Santo\(^{19}\), Arthur Ernst\(^{9,20}\), Pedro M. Echenique\(^{2,7,8}\), Nazim T. Mamedov\(^{11}\), Alexander M. Shikin\(^1\) and Eugene V. Chulkov\(^{1,2,7,8}\)

Feasibility of many emergent phenomena that intrinsic magnetic topological insulators (TIs) may host depends crucially on our ability to engineer and efficiently tune their electronic and magnetic structures. Here we report on a large family of intrinsic magnetic TIs in the homologous series of the van der Waals compounds \((\text{MnBi}_2\text{Te}_4)(\text{Bi}_2\text{Te}_3)_m\) with \(m = 0, \ldots, 6\). Magnetic, electronic and, consequently, topological properties of these materials depend strongly on the \(m\) value and are thus highly tunable. The antiferromagnetic (AFM) coupling between the neighboring Mn layers strongly weakens on moving from \(\text{MnBi}_2\text{Te}_4\) \((m = 0)\) to \(\text{MnBi}_4\text{Te}_7\) \((m = 1)\) and \(\text{MnBi}_8\text{Te}_{10}\) \((m = 2)\). Further increase in \(m\) leads to change of the overall magnetic behavior to ferromagnetic (FM) one for \((m = 3)\), and the interlayer coupling almost disappears. In this way, the AFM and FM TI states are, respectively, realized in the \(m = 0, 1, 2\) and \(m = 3\) cases. For large \(m\) numbers a hitherto-unknown topologically nontrivial phase can be created, in which below the corresponding critical temperature the magnetizations of the non-interacting 2D ferromagnets, formed by the \(\text{MnBi}_4\text{Te}_7\) building blocks, are disordered along the third direction. The variety of intrinsic magnetic TI phases in \((\text{MnBi}_2\text{Te}_4)(\text{Bi}_2\text{Te}_3)_m\) allows efficient engineering of functional van der Waals heterostructures for topological quantum computation, as well as antiferromagnetic and 2D spintronics.

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INTRODUCTION

Magnetism and topology can meet each other both in real space, giving rise to complex magnetic structures such as vortices or skyrmions, and in reciprocal momentum space, resulting in Weyl semimetal or magnetic topological insulator (MTI) phases. In the MTI case, the interplay between topology and magnetism provides particularly rich playground for realization of exotic physics. Below the magnetic critical temperature, the time-reversal symmetry breaks down introducing a mass term to the linear dispersion of Dirac fermions thus opening opportunities for symmetry breaks down introducing a mass term to the linear dispersion of Dirac fermions thus opening opportunities for

Until recently, the magnetism in topological insulators (TIs) has been achieved using either magnetic doping\(^{14,12,16}\), or proximity effect\(^{17,18}\) as well as by construction of van der Waals (vdW) heterostructures\(^{19-23}\). This situation has changed drastically with the recent discovery of the AFM TI phase\(^{24}\) in stoichiometric vdW-layered antiferromagnet \(\text{MnBi}_2\text{Te}_7\)\(^{25-29}\), which inspired a lot of research activity as it holds promise for realization of the high-temperature QAH and axion insulator states, Majorana hinge modes and other effects\(^{24,26-28,30-34}\).

Here we propose the MTI family by introducing the \((\text{MnBi}_2\text{Te}_4)(\text{Bi}_2\text{Te}_3)_m\) series of vdW materials that, apart from \(\text{MnBi}_2\text{Te}_4\) \((m = 0)\), contains six more topologically nontrivial compounds, namely \(\text{MnBi}_4\text{Te}_7\) \((m = 1)\), \(\text{MnBi}_{8}\text{Te}_{10}\) \((m = 2)\), \(\text{MnBi}_{10}\text{Te}_{13}\) \((m = 3)\), \(\text{MnBi}_{10}\text{Te}_{16}\) \((m = 4)\), \(\text{MnBi}_{12}\text{Te}_{19}\) \((m = 5)\), and \(\text{MnBi}_{12}\text{Te}_{22}\) \((m = 6)\). Along the series, the strength of the interlayer exchange interaction, that couples neighboring FM Mn layers, gradually decreases with the increase of \(m\), while the overall magnetic ordering changes from an AFM \((m = 0, 1, 2)\) to FM \((m = 3)\). Combined with the non-trivial topology of the \((\text{MnBi}_2\text{Te}_4)(\text{Bi}_2\text{Te}_3)_m\) compounds, these magnetic states give rise to the AFM and FM TI phases for \(m = 0, 1, 2\) and \(m = 3\), respectively. For large \(m\) numbers a new MTI phase can be formed in which, below the respective \(T_C\), the magnetizations of the 2D AFM-ordered Mn layers of the \(\text{MnBi}_4\text{Te}_7\) building blocks are disordered along the [0001]
direction. The topologically nontrivial nature of these compounds is confirmed by angle-resolved photoemission spectroscopy (ARPES) measurements that reveal the presence of the topological surface states (TSS) whose dispersion depends strongly on the crystal surface termination. The unusual magnetic properties make the \((\text{MnBi}_2\text{Te}_3)(\text{Bi}_2\text{Te}_3)_m\) series a unique tunable platform for creating various exotic states of matter, such as intrinsic axion or QAH insulator\(^{20,26,32}\), the field-induced QH phase\(^{31,32}\), high-order Möbius insulator\(^{35}\), or chiral topological superconductor\(^{39}\).

**RESULTS AND DISCUSSION**

**CRYSTAL STRUCTURE AND MAGNETIC CROSSOVER**

The first compound in the \((\text{MnBi}_2\text{Te}_3)(\text{Bi}_2\text{Te}_3)_m\) series is \(\text{MnBi}_2\text{Te}_4\) \((m = 0)\), which had been investigated previously and discovered to be the first AFM Ti\(^{25,36}\). This system consists of septuple layer (SL) blocks stacked one on top of another. Each SL is a 2D ferromagnet, while the coupling between the neighboring SLs is AFM\(^{25,37}\). For \(m \geq 1\), the members of the \((\text{MnBi}_2\text{Te}_3)(\text{Bi}_2\text{Te}_3)_m\) family are comprised of alternating septuple \((\text{MnBi}_2\text{Te}_4)\) and quintuple \((\text{Bi}_2\text{Te}_3)\) layer blocks (see Fig. 1a). The growth details and crystal structures of thus-formed \(\text{MnBi}_4\text{Te}_7\) and \(\text{MnBi}_{10}\text{Te}_{16}\) compounds have been first reported in ref. \(^{38}\), for which the -5-7-5-7- and -5-5-7-5-7- blocks sequences corresponding to \(m = 1\) and \(m = 2\) have been discovered, respectively.

The XRD patterns of our \(\text{MnBi}_4\text{Te}_7\), \(\text{MnBi}_{10}\text{Te}_{16}\), \(\text{MnBi}_8\text{Te}_{13}\), \(\text{MnBi}_{10}\text{Te}_{16}\), \(\text{MnBi}_{12}\text{Te}_{19}\), and \(\text{MnBi}_{14}\text{Te}_{22}\) samples, shown in Supplementary Fig. 1, confirm their \(P3m1\) and \(R3m\) space groups.

The temperature dependence of the resistivity measured in a zero magnetic field demonstrates the metallic-like behavior for both \(\text{MnBi}_4\text{Te}_7\) and \(\text{MnBi}_{10}\text{Te}_{16}\) (see Fig. 1b, c). At low temperatures, the well-defined kinks at 13.2 K \((\text{MnBi}_4\text{Te}_7)\) and 11.9 K \((\text{MnBi}_{10}\text{Te}_{16})\) are observed for both compounds. As the external magnetic field is switched on and increased these features are washed out, pointing towards their magnetic origin.

The field-cooled (FC) and zero-field cooled (ZFC) magnetic susceptibilities measured at 0.1 T for \(\text{MnBi}_4\text{Te}_7\) are shown in Fig. 1d (blue curve). The high temperature paramagnetic behavior ends up with a pronounced peak at 13 K, that is characteristic of an AFM ordering. The fitting of the susceptibility by the Curie–Weiss law yields the Curie–Weiss temperature \((\Theta_{\text{CW}})\) of 13.2 K. Positive sign and relatively high value of \(\Theta_{\text{CW}}\) (cf. 3–6 K for \(\text{MnBi}_4\text{Te}_4\)) indicate the presence of strong ferromagnetic interactions in \(\text{MnBi}_4\text{Te}_7\), in spite of the overall AFM behavior. The Néel temperature of only 13 K for \(\text{MnBi}_4\text{Te}_7\), versus 25 K for \(\text{MnBi}_4\text{Te}_4\), reveals a strong weakening of the interlayer AFM coupling due to the insertion of the non-magnetic quintuple layer block (QL) between neighboring SLs. The onset of the

![Figure 1](https://example.com/figure1.png)

**Fig. 1** a Compounds \((\text{MnBi}_2\text{Te}_3)(\text{Bi}_2\text{Te}_3)_m\) consist of alternating five-layer (QL) and magnetic seven-layer (SL) blocks. b, c Temperature dependence of the resistivity for \(\text{MnBi}_4\text{Te}_7\) and \(\text{MnBi}_{10}\text{Te}_{16}\) for various applied out-of-plane magnetic fields. d Normalized magnetic susceptibility for \(\text{MnBi}_4\text{Te}_7\), \(\text{MnBi}_{10}\text{Te}_{16}\), \(\text{MnBi}_8\text{Te}_{13}\), and \(\text{MnBi}_{10}\text{Te}_{16}\) as a function of temperature measured in a small magnetic field in zero-field-cooled and field-cooled conditions. d, e Field-dependent magnetization curves taken at various temperatures with out-of-plane external magnetic field for \(\text{MnBi}_4\text{Te}_7\), \(\text{MnBi}_{10}\text{Te}_{16}\), \(\text{MnBi}_8\text{Te}_{13}\), and \(\text{MnBi}_{10}\text{Te}_{16}\).
ferromagnetic interactions is also manifested in splitting of the FC and ZFC curves at low temperature (spin-glass-like transition).

Increasing by one the number of QLS between SLs and forming MnBi$_{10}$Te$_{16}$ leads to further weakening of the interlayer exchange interaction. The magnetic susceptibility data for this compound, shown in Fig. 1d (red curve), exhibit similar cusps at low temperature, signaling the AFM ordering, but the Néel temperature decreases to 11 K in this case. Furthermore, below 10 K FC and ZFC curves splitting becomes larger than for MnBi$_2$Te$_7$, thus showing the enhanced competition between AFM and FM couplings.

The $m = 3$ and 4 members of the series, i.e. MnBi$_{6}$Te$_{10}$ and MnBi$_{10}$Te$_{16}$, show an overall ferromagnetic behavior below the Curie temperatures of about 12 K, as revealed by the magnetization measurements (Fig. 1d); a similar behavior is expected for MnBi$_{11}$Te$_{19}$ ($m$ = 5) and MnBi$_{14}$Te$_{22}$ ($m$ = 6) because of the vanishing interlayer exchange interaction.

The $M(H)$ curves for $m = 1$–$4$ compounds taken at various temperatures are presented in Fig. 1e–g. Slightly below the Néel temperature (10 K) for MnBi$_2$Te$_7$, a typical AFM $M(H)$ behavior takes place, with a spin–flip upturn appearing at 0.2 T, the latter value being much lower than that for MnBi$_{12}$Te$_{25}$ (3.5 T). The gradual reduction of interlayer exchange interaction leads to further decrease of this value, the $M(H)$ dependence for MnBi$_{10}$Te$_{16}$ compound (red curve in Fig. 1e) exhibits the spin–flip transition at about $-0.07$ T. The next members of the MBT family, i.e. MnBi$_{13}$Te$_{19}$ and MnBi$_{14}$Te$_{22}$ demonstrate rather conventional ferromagnetic s-like curves.

At very low temperatures ($T = 5$ and 2 K), the spin–flip hysteresis opens up in the magnetic field interval from 0.1 to 0.3 T for $m = 1$ system, as seen in Fig. 1f, g. The $m = 2$ compound exhibits the same behavior, but at lower external fields. Moreover, at 2 K, in the absence of external field, the magnetization does not fall to zero and forms a ferromagnetic hysteresis loop with small and large remanence for $m = 1$ and 2, respectively. Such a dual complex metamagnetic behavior can be explained by the presence of domains with ferromagnetic and AFM ordering between neighbor SLs. However, in case of $m = 2$ the remanence close to saturation shows that forced FM state can survive at zero and even at small negative magnetic fields when the thermal fluctuations are weak enough. Similar results with the metamagnetic behavior of MnBi$_2$Te$_7$ and MnBi$_{10}$Te$_{16}$ have been reported recently in ref. 39. The $m = 3$ (MnBi$_{11}$Te$_{19}$) compound clearly demonstrates an almost pure ferromagnetic hysteresis loop with small and large remanence for $m = 1$ and 2, respectively. Such a dual complex metamagnetic behavior can be explained by the presence of domains with ferromagnetic and AFM ordering between neighbor SLs. However, in case of $m = 2$ the remanence close to saturation shows that forced FM state can survive at zero and even at small negative magnetic fields when the thermal fluctuations are weak enough. Similar results with the metamagnetic behavior of MnBi$_2$Te$_7$ and MnBi$_{10}$Te$_{16}$ have been reported recently in ref. 39.

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To separate the bulk and surface states, ARPES measurements with various photon energies (50, 18, and 6.3 eV (laser)) have been performed, as presented in Supplementary Fig. 6. The dispersion of the linear band does not show any photon energy dependence, which points towards its surface or 2D character. This allows suggesting that the linear band is the TSS, while far from the $\Gamma$-point the TSS is likely to be the trivial surface state in the valence band that interacts with the TSS near the $\Gamma$-point, leading to the appearance of the “avoided crossing” gap at the BE of 0.29 eV. In this case, the degeneracy point between the M-band and the close-lying hole band can be identified as the Dirac point (DP) of the MnBi$_{13}$Te$_{22}$ (0001) TSS.

**TOPOLOGICAL SURFACE STATES**

We now turn to the electronic structure study of the compounds in the (MnBi$_2$Te$_4$)(Bi$_2$Te$_3$)$_m$ series. As it has been mentioned above, the ARPES dispersion relations for the (0001) surface of the MnBi$_2$Te$_4$ compound ($m = 0$) measured at $T = 60$ K are shown in Fig. 2a. Within the binding energy (BE) window from 0.5 to 4 eV, a quite complex band structure, characteristic of bismuth chalcogenides is seen. However, unlike nonmagnetic TIs, a weakly dispersive state is discernible in Fig. 2a at the BE of about 3.8 eV, which is attributed to the Mn 3d-states, whose intensity is enhanced at the Mn-resonant photon energy of 50 eV.
Since the TSS should be spin-polarized, spin-ARPES measurements have been performed. The acquired spectra (Supplementary Fig. 6) clearly demonstrate the spin polarization reversal for opposite branches of the linear band, revealing the characteristic helical spin texture of the TSS. The performed bands assignment allows us to estimate the bulk band gap of MnBi$_4$Te$_7$ to be about 0.15 eV. It should be noted that on the surface of MnBi$_4$Te$_7$, since it is built of two different crystal blocks, QL and SL, two surface terminations and, consequently, two Dirac TSSs with different dispersion are expected. The TSS signal for each termination has been obtained by means of laser-ARPES and will be analyzed below.

According to the DFT electronic structure calculations, AFM bulk MnBi$_4$Te$_7$ features a fundamental band gap of 0.18 eV (Supplementary Note 3). Because of its interlayer AFM ordering, MnBi$_4$Te$_7$ is invariant with respect to the combination of the time-reversal ($\Theta$) and primitive-lattice translation ($T_{123}$) symmetries, $S = \Theta T_{123}$, and thus obeys the $Z_2$ topological classification of AFM insulators$^{24,49}$. We find $Z_2 \neq 1$ for MnBi$_4$Te$_7$, meaning that its fundamental band gap is inverted whereby, similarly to MnBi$_4$Te$_{10}$, MnBi$_4$Te$_7$ is an AFM TI below the Néel temperature. The AFM TI state of MnBi$_4$Te$_7$ along with the out-of-plane direction of the staggered magnetization’s easy axis dictate that there should be a gapped (gapless) TSS at the $S$-breaking ($S$-preserving) surface. This is exactly what we find: the TSS is gapped at both of the possible terminations of the MnBi$_4$Te$_7$(0001) surface, which is $S$-breaking. At the SL termination, the DP gap is located inside the fundamental bulk band gap and reaches a large value of 70 meV (Fig. 2c). At the QL termination, a more complex surface electronic structure is revealed, with four bands located in the region of interest. To understand this spectrum, we have performed surface electronic structure calculations at different spin–orbit coupling (SOC) strengths. As it can be seen in Supplementary Fig. 10, with no SOC included there is an exchange-split trivial surface state in the valence band’s projected band gap around the Γ-point at energy of about $-0.3$ eV. When the SOC is turned on and the system is in the topological phase, this spin-split state interacts with the TSS of the QL-termination, leading to the appearance of avoided crossings (Supplementary Fig. 10).

At the natural SOC strength (Fig. 2c), these avoided crossing effects are quite significant and the Dirac cone appears to be torn into two parts, one of which is located in the fundamental band gap, while another in the projected band gap between approximately $-0.1$ and $-0.2$ eV. The split DP of the QL termination lies at about 0.16 eV below the Fermi level. The smaller DP gap size at the QL termination (about 29 meV) is caused by the predominant localization of the TSS in the surface.

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**Fig. 2** a, d ARPES dispersion relations for the large energy and momentum region of MnBi$_4$Te$_7$ and MnBi$_4$Te$_{10}$ taken at 60 K at a photon energy of 50 eV. b, e ARPES dispersion relations of the Dirac cone region taken at a photon energy of 30 eV at 60 K (BCB (BVB) denotes bulk conduction (valence) band). c DFT-calculated layer-resolved electronic structure of the MnBi$_4$Te$_7$(0001) surface. The size of color circles reflects the weight of the state in the topmost block of the SL (green) and QL (blue) termination. The orange circles show the contribution of the subsurface SL block of the QL termination. The gray shadings correspond to the bulk band structure projected onto the 2D Brillouin zone. The same for MnBi$_6$Te$_{10}$(0001) surface, the size of green, blue, and red circles reflects the weight of the state in the topmost block of the 7-5-, 5-7-5-, and 5-5-7- terminations, respectively.
located in the surface QL block and therefore its DP is almost unsplit.

In order to experimentally separate various terminations of MnBiTe$_2$ and MnBi$_{10}$Te$_{10}$, we used laser-based ARPES technique that spatial resolution is up to ~5 μm$^2$, while for synchrotron-based measurements (Fig. 2) the resolution is up to ~100 μm. In Fig. 3 the corresponding dispersion relations are presented for two (upper panels) and three (lower panels) terminations of MnBi$_2$Te$_2$ and MnBi$_{10}$Te$_{10}$ respectively. In contrast to the synchrotron-based measurements the SL-terminated Dirac cone for MnBi$_2$Te$_2$ has been revealed (Fig. 3a). Spectra from QL terminated surfaces (5-7-, 5-7-5- and 5-5-7-; see Fig. 3b, e, f), correspondingly are in good agreement with theoretical predictions and synchrotron measurements (see Fig. 2), as well as with the recent experimental works$^{53-55}$. The distinct DP positions can be easily determined for 5-7-5- and 5-5-7- terminations of MnBi$_2$Te$_2$, which has larger BE for 5-7-5- termination, in accordance with the theory.

The electronic structure of SL terminated surfaces of MnBi$_2$Te$_2$ and MnBi$_{10}$Te$_{10}$ (Fig. 3a, d) have similar features and the most important is the Dirac cone, located within the bulk band gap, with the DP at ~0.28 eV of BE, in agreement with the DFT-derived band structure (Fig. 2c, f). Nevertheless, besides the Dirac cone and bulk bands the laser-based spectra exhibit the wide parabolic-like state, dispersing from ~0.25 eV at the Γ-point to the Fermi level at ~0.17 Å$^{-1}$ that is absent in ab initio calculations (see Fig. 2c, f and refs. $^{56,57}$). Similar band dispersions for SL-terminated terrace have been observed in refs. $^{54,56,57}$. The origin of the parabolic-like band is under debates currently. Since ab initio calculations cannot reproduce this electronic band, its origin can lie in the deviations of the surface structure from the ideal one. As an example, recently the dramatic effect of small variation of the near surface vdW gap on the band structure of MnBi$_2$Te$_4$(0001) has been demonstrated$^{58}$. In refs. $^{56,57}$ the idea of Rashba-like surface state on SL-termination is proposed. Indeed, surface localization of the band can be confirmed since it exists only in SL-terminations and it does not appear for QL-terminated surfaces (Fig. 3b, e, and f). The ARPES Fermi surface (Fig. 3c) exhibits a weak hexagonal warping of the band and absence of the interaction with the bulk conduction band states. Notably, similar band was not observed for SL-terminated surfaces in structurally similar compounds PbBi$_2$Te$_2$ and PbBi$_{10}$Te$_{10}$$^{59,60}$. One also can notice that spectra for SL-termination in MnBi$_2$Te$_2$ and MnBi$_{10}$Te$_{10}$ slightly differ in the valence band region, where interaction of the lower part of the Dirac cone with the bulk bands is seen for the case of MnBi$_{10}$Te$_{10}$.

Finally, the electronic structure measurements performed for the MnBi$_2$Te$_3$(0001) and MnBi$_{10}$Te$_{10}$(0001) surfaces reveal the presence of the TSSs within the bulk band gap too (see Supplementary Figure 5), but their analysis is complicated due to increased number of surface terraces after the cleavage. Thus, all the compounds of the presented (MnBi$_m$Te$_2$)(Bi$_2$Te$_3$)$_m$ family are magnetic TIs, whose topological class changes with $m$. While MnBi$_2$Te$_4$, MnBi$_4$Te$_7$, and MnBi$_6$Te$_{10}$ ($m = 0, 1, 2$) are 3D AFM TIs, MnBi$_{11}$Te$_{13}$ ($m = 3$) turns out to be a FM TI with weak interlayer exchange coupling. For $m > 3$ no signatures of the interlayer exchange interaction could be detected in our experiments, which has a very interesting consequence: MnBi$_{11}$Te$_{13}$, MnBi$_{13}$Te$_{15}$, and MnBi$_{15}$Te$_{17}$ could be the first examples of stoichiometric 3D MTI compounds in which the magnetizations of the 2D FM-ordered layers are disordered along the [0001] direction below the corresponding critical temperature. Similar idea has been discussed in ref. $^{60}$ where starting from $m = 3$ the so-called "single layer magnet" phase is proposed.

The peculiar magnetic properties of the (MnBi$_m$Te$_2$)(Bi$_2$Te$_3$)$_m$ family combined with the nontrivial topology of its constituents enable observation of interesting effects for all of the presented members of the series. Those effects would take advantage of the interlayer exchange coupling tunability along the series, which is
feasible through the changing of the number of QLs separating the SLs. This allows one to tailor both the strength and character of the interlayer exchange coupling and even to switch it off for large \( m \) numbers. One particular consequence of it is that the magnetic structure, and therefore the topological class of the compounds can be tuned by an external magnetic field. This property is especially attractive in the 2D limit, where the \([\text{MnBi}_2\text{Te}_4]_{1\text{SL}}/(\text{Bi}_2\text{Te}_3)_{\text{nQLs}}/([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}\text{SL})\) sandwiches, that can be obtained by careful exfoliation of the thin flakes from the single crystal surface\(^{31,32}\), turns to either the intrinsic zero plateau QAH state (also known as the axion insulator state) or the Chern insulator state. For \( m \leq 3 \), the latter state can be achieved in zero external magnetic field as has been earlier predicted by theory\(^{13}\), while for \( \text{MnBi}_2\text{Te}_4 \) and, probably, for \( \text{MnBi}_4\text{Te}_7 \) an external magnetic field is needed to achieve the quantized Hall effect\(^{31,32}\). However, in the \( \text{MnBi}_4\text{Te}_7 \) and \( \text{MnBi}_6\text{Te}_{10} \) compounds, the strength of the critical field needed to overcome the AFM interlayer exchange coupling should be much smaller than that used for \( \text{MnBi}_2\text{Te}_4 \). The latter fact has also been pointed out as an advantage for a possible realization of the topological superconductor state based on the \([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}/(\text{Bi}_2\text{Te}_3)_{m \text{QLs}}\text{SL}\) family, hosting the exotic Majorana fermions\(^{33}\). From this point of view, the \([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}/(\text{Bi}_2\text{Te}_3)_{m \text{QLs}}\text{SL}\) series represents a unique and highly tunable topological van-der-Waals platform for creation of both exotic topological phases and functional devices for AFM and 2D spintronics as well as for topological quantum computing.

In summary, we have reported the magnetic topological insulators (MTIs) family \([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}/(\text{Bi}_2\text{Te}_3)_{m \text{QLs}}\text{SL}\) consisting of Mn-based magnetic SL blocks separated by different number \( m \) of non-magnetic quintuple layers. The interlayer exchange coupling between the neighboring SLs can be tuned by changing \( m \) giving rise to a crossover from the interlayer AFM ordering for \( m = 0, 1, 2 \) \([\text{MnBi}_2\text{Te}_4, \text{MnBi}_4\text{Te}_7 \text{, and MnBi}_6\text{Te}_{10}]\) to the overall ferromagnetic one for \( m = 3 \) \([\text{MnBi}_9\text{Te}_{10}]\) and, finally, to almost complete disappearance of the interlayer interaction for \( m > 3 \) \([\text{MnBi}_{10}\text{Te}_{16}, \text{MnBi}_{12}\text{Te}_{19}, \text{and MnBi}_{14}\text{Te}_{22}]\). Combined with a non-trivial topology of the \([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}/(\text{Bi}_2\text{Te}_3)_{m \text{QLs}}\text{SL}\) compounds, proven by ARPES, these magnetic states give rise to the AFM and FM TI phases for \( m = 0, 1, 2 \) and \( m = 3 \), respectively, while for \( m > 3 \) a new MTI phase could be formed in which, below \( T_c \), the magnetizations of the 2D FM-ordered Mn layers of the \( \text{MnBi}_2\text{Te}_4 \) building blocks are disordered along the [0001] direction. Depending on the surface terminations, a complex bundle of the Dirac cones is resolved by means of DFT and ARPES. The tunable magnetic and topological phases in \([\text{MnBi}_2\text{Te}_4]_{1\text{QLs}}/(\text{Bi}_2\text{Te}_3)_{m \text{QLs}}\text{SL}\) series allow engineering the promising platforms not only for QAH effect, axion insulators, and Majorana fermions, but also for emerging fields of AFM and van-der-Waals 2D spintronics.

**METHODS**

Magnetic and transport measurements

Magnetic measurements were carried out in the resource center “Center for Diagnostics of Materials for Medicine, Pharmacology and Nanoelectronics” of the SPbU Science Park using a SQUID magnetometer with a helium cryostat manufactured by Quantum Design. The experiments were carried out in a pull mode in terms of temperature and magnetic field. The applied magnetic field was perpendicular to the (0001) sample surface. Transport measurements were done with a standard four-probe ac technique using a low-frequency (f \( \approx \) 20 Hz) Lock-in amplifier. Contacts were attached with conducting graphite paste. The experiments were carried out in a temperature-variable cryostat at different values of magnetic field up to 8 T, generated by a superconducting solenoid and directed along the normal to the (0001) sample surface.
Photoemission measurements

The experiments were carried out at 1-cubed UE-112 beamline at BESSY II in Berlin, BaDEiPh beamline at Elettra synchrotron in Trieste (Italy), BL-1, BL-9, and laser ARPES endstation at HISOR in Hiroshima, and at Research Resource Center of St. Petersburg State University “Physical methods of surface investigation” with a Scienta R4000 or a Specs Phoibos 150 energy analyzer. Samples were cleaved in situ at the base pressure of 6 × 10⁻¹⁰ mbar. The crystalline order and cleanliness of the surface were checked by low-energy electron diffraction (LEED) and X-ray photoelectron spectroscopy (XPS). Spin-resolved ARPES measurements were performed at BL-9 beamline of HISOR synchrotron in Hiroshima and APE beamline at Elettra synchrotron in Trieste (Italy). The spectra were measured using VLEED spin detector. Total energy and angular resolutions were 20 meV and 1.5°, respectively.

Electronic structure and total energy calculations

Electronic structure calculations were performed using the density functional theory and the projector-augmented wave (PAW) method, realized in the VASP code. The exchange-correlation potential was described within the generalized gradient approximation in the Perdew–Burke–Ernzerhof formulation (GGA-PBE). The Hamiltonian contained scalar relativistic corrections and the SOC was taken into account self-consistently. We used the DFT-D2 and the DFT-D3 approaches to describe the vdW interactions, that yielded similar results. The plane-wave energies up to 270 eV were used for the wave function expansions. Structural relaxations were done until the forces on atoms were smaller than 0.01 eV/Å. Depending on the particular task and geometry, different grids for the BZs sampling were used (see below), all of them being Γ-centered.

The Mn 3d-states were described using the GGA + U method as formulated by Dudarev et al. The Uₜₜ = U – Jₜ value for the Mn 3d-states was chosen to be equal to 5.34 eV, as in previous works on MnBi₂Te₄. The bulk magnetic ordering was studied using total-energy calculations, performed for the FM and two different AFM states. Namely, we considered an interlayer AFM state and a noncollinear (NCL) intralayer AFM state, in which three spin sublattices form angles of 120° with respect to each other. To model the FM and interlayer AFM structures in MnBi₆Te₁₀ and MnBi₄Te₁₀, we used cells with 24 and 34 atoms, respectively. For the MnBi₂Te₄ system, these calculations were performed with the respective 3D BZs sampled by the 25 × 25 × 5 × 5 k-point grids. For the MnBi₂Te₁₀ compound, which exhibits extremely weak interlayer exchange coupling, the interlayer ordering was carefully studied using very fine k-meshes up to 23 × 23 × 19 points. These meshes were also used in the magnetic anisotropy energy calculations. For MnBi₂Te₄, the NCL intralayer AFM configuration was treated using hexagonal bulk cell containing three atoms per layer (sqrt(3) × sqrt(3) R30° in-plane periodicity) and a 11 × 11 × 3 BZ sampling. For MnBi₂Te₁₀, NCL configuration has not been considered since all the available experimental and theoretical data in the literature indicate that each MnBi₂Te₄ SL block orders ferromagnetically, irrespectively of its structural environment.

The MnBi₂Te₄ and MnBi₄Te₁₀ semi-infinite surfaces were simulated within a model of repeating slabs separated by a vacuum gap of at least 10 Å. The interplanar distances were optimized for the utmost SL or QL block of each surface. The structural relaxations and static electronic structure calculations were performed using a k-point mesh of 11 × 11 × 1 in the 2D BZ. The procedures of the magnetic anisotropy energy calculations and Monte Carlo simulations are described in detail in ref. 25.

Exchange coupling constants calculations

For the equilibrium atomic structure of MnBi₂Te₄, obtained with VASP, we calculated the Heisenberg exchange coupling constants Jₜₜ, ab initialized using the full-potential linearized augmented plane waves (FLAPW) method in the FLEUR implementation (http://www.fleur.de). In the Jₜₜ calculations SOC was neglected. We took the GGA+U approach under the fully localized limit, using similar settings as those in refs. 25,26. For the self-consistent FLAPW basis set, the plane waves were constructed with a 18 × 18 × 4 Monkhorst-Pack k-point sampling of the first BZ and cut-off energies of 3.4 Hartrees for the wavefunctions and 10.4 Hartrees for the density and potential expansions. Muffin tin sphere radius was set to 2.74 a.u., for Mn, while a value of 2.81 a.u. was used for Bi and Te, and the partial wave functions were expanded up to l = 8. Mn, Bi, and Te contributed 4s3d, 5s5p, and 6s6p valence electrons, respectively.

The Jₜₜ constants were extracted by Fourier inversion of spin spirals in the reciprocal cell characterized by the q vectors of a 19 × 19 × 3 grid. These dispersion energies, calculated in the force theorem approach, converged below 0.1 meV and allowed adding up to 150 magnetic coordination spheres to the Fourier analysis.

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Author Contributions
I.U. and M.M.O. have written the manuscript and contributed as co-first authors. The ARPES measurements were carried out by I.U., A.M.S., D.E., V.V., S.O.F., A.G.R., G.D.S., L.P., A. Kimura. The SQUID magnetometry has been done by A. Koroleva and E. S. The samples have been grown and characterized by Z.S.A., M.B.B., I.R.A., O.E.T., and G.D.S., L.P., A. Kimura. The SQUID magnetometry has been done by A. Koroleva and E. S. The exchange coupling constants calculations were performed by M.B.-R., M.M.O., and G.D.S. The transport measurements have been carried out by N.M., N.A.A., and V.N.Z. The band structure calculations were performed by M.M.O., M.B.-R., S.V.E., and E.V.C. The exchange coupling constants calculations were performed by M.B.-R., M.M.O., and G.D.S. The tight-binding calculations were performed by I.P.R. The magnetic anisotropy studies were performed by M.M.O. The Monte Carlo simulations were performed by M.H. The supervision of the project was executed by E.V.C.

Competing Interests
The authors declare no competing interests.
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Correspondence and requests for materials should be addressed to I.I.K., M.M.O. or E.V.C.

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