Thermodynamic approach for enhancing superconducting critical current performance

Masashi Miura1,2,3, Go Tsuchiya1, Takumu Harada1, Keita Sakuma1, Hodaka Kurokawa4, Naoto Sekiya5, Yasuyuki Kato6, Ryuji Yoshida7, Takeharu Kato7, Koichi Nakaoka8, Teruo Izumi8, Fuyuki Nabeshima4, Atsutaka Maeda4, Tatsumori Okada9, Satoshi Awaji9, Leonardo Civale2 and Boris Maiorov6

Abstract

The addition of artificial pinning centers has led to an impressive increase in the critical current density ($J_c$) of superconductors, enabling record-breaking all-superconducting magnets and other applications. The $J_c$ of superconductors has reached ~0.2–0.3 $J_d$, where $J_d$ is the depairing current density, and the numerical factor depends on the pinning optimization. By modifying $\lambda$ and/or $\xi$, the penetration depth and coherence length, respectively, we can increase $J_d$. For ($Y_{0.7}$Gd$_{0.3}$)Ba$_2$Cu$_3$O$_{6+x}$, we can achieve this by controlling the carrier density, which is related to $\lambda$ and $\xi$. We can also tune $\lambda$ and $\xi$ by controlling the chemical pressure in Fe-based superconductors, i.e., BaFe$_2$(As$_1$–xP$_x$)$_2$ films. The variation in $\lambda$ and $\xi$ leads to an intrinsic improvement in $J_c$ via $J_d$, allowing extremely high values of $J_c$ of 130 MA/cm$^2$ and 8.0 MA/cm$^2$ at 4.2 K, consistent with an enhancement in $J_d$ of a factor of 2 for both incoherent nanoparticle-doped ($Y$,Gd)$_{123}$ coated conductors (CCs) and BaFe$_2$(As$_{1–x}$P$_x$)$_2$ films, showing that this new material design is useful for achieving high critical current densities in a wide array of superconductors. The remarkably high vortex-pinning force in combination with this thermodynamic and pinning optimization route for the ($Y$,Gd)$_{123}$ CCs reached ~3.17 TN/m$^3$ at 4.2 K and 18 T (H||c), the highest values ever reported for any superconductor.

Introduction

High-temperature superconductors are attractive because their high critical temperature ($T_c$) enables them to be used at high temperature and outperform standard superconductors in terms of magnetic field performance. However, the limiting factor is the ability to arrest the motion of Abrikosov vortices at a very high critical current. The dissipative motion of vortices can be reduced or eliminated by pinning at nonsuperconducting defects. There are several possible approaches for enhancing the critical current density. Over the last three decades, enormous improvements in the properties of the oxide high-temperature superconductors (HTSs) of the REBa$_2$Cu$_3$O$_y$ family (RE123) have mostly been achieved by adding and tailoring pinning centers to immobilize vortices. The number of routes for engineering the pinning landscape to increase $J_c$ is too large to describe and continues to be fruitful. The creep-free $J_c$, $J_{c0}^\text{NPs}(T,H)$, for strong pinning by nanoparticles ($D_{np} \geq 2\xi$) is expressed as

$$J_{c0}^\text{NPs} \propto N_{np} \mu_0 H^2 \pi^2 \frac{\xi^2 D}{4\xi} \propto N_{np} \left( \frac{1}{\lambda^2} \right)$$

where $N_{np}$ is the density of the nanoparticles (NPs), $D$ is the mean size of the NPs, $\xi$ is the coherence length, $\lambda$ is the London penetration depth, and $H_c$ is the thermodynamic critical field (see SI, Section 1). How close $J_c$ can be to the upper limit of $J_{c0}$, i.e., the depairing current density ($J_d$), by the addition of pinning centers is...
still an open question. The $J_d$ within the Ginzburg-Landau theory is

$$J_d(T) = \frac{2\sqrt{2}H_c(T)}{3\sqrt{3}\lambda_{ab}(T)} \frac{\phi_0}{3\sqrt{3}\pi\mu_0\lambda_{ab}(T)^2\xi_{ab}(T)} \propto \left(\frac{1}{\lambda^2\xi}\right)$$

(2)

where $\phi_0$ is the flux quantum.

Experimentally, the enhancement in $J_c$ by tuning the carrier density, especially in standard RE123 films, i.e., without artificial pinning centers (APCs), has been reported. Recently, A. Stangl et al. reported that overdoped standard Y123 films grown by pulsed laser deposition (PLD) attained 18% $J_d$ at 5 K, which is a consequence of the increase in condensation energy with charge carrier density. On the other hand, by adding and tailoring APCs, the highest $J_c$ achieved for RE123 and Fe-based films is in the range of 10–20% $J_d$. Most of the studies introducing APCs into RE123 are on coherent BaMO$_3$ (BMO, $M = Zr, Hf, Sn$, etc.) nanorods and coherent Y$_2$BaCuO$_5$ precipitates. The $c$ axis of the RE123 matrix is expanded by coherent APCs, resulting in a reduced carrier density due to strain-induced oxygen-vacancy formation and decreased crystallinity. On the other hand, we have succeeded in introducing incoherent BMO NPs into not only (Y$_{0.77}$Gd$_{0.23}$)Ba$_2$Cu$_3$O$_{6+\delta}$ (Y,Gd) 123) films but also Fe-based pnictide BaFe$_2$(As$_{1-x}$P$_x$)$_2$ (Ba122:P) films, which leaves the matrix unaltered with just slightly decreased superconducting properties. The BaHfO$_3$ (BHO) NPs in RE123 films and BrZrO$_3$ (BZO) NPs in Ba122:P films have an average size ($D_{ave}$) of 7 nm with a density $N_{np} \sim 80 \times 10^{21}$ m$^{-3}$ and $D_{ave}$ of 8 nm with $N_{np} \sim 68 \times 10^{21}$ m$^{-3}$, respectively. For both nanocomposite materials, we have shown a large enhancement in $J_c$ at not only self-field but also in-field by introducing a high density of incoherent NPs of a tailored size. Theoretically, using the time-dependent Ginzburg-Landau equations (TDGL) and a targeted evolution approach, Sadovskyy et al. explored the optimization of $J_c$, showing that a level of 30–40% $J_d$ could be attained.

Now, in addition to focusing on improving the pinning morphology, we can increase $J_d$. Considering Formulas (1) and (2), we see that $J_d \propto \left(\frac{T_c}{T}\right)^{2} \propto \lambda_{g}$. Therefore, reducing $\lambda$ or $\lambda$ would improve $J_d$ and consequently $J_c$. However, these parameters are material-specific and have not been thoroughly studied for improving the $J_c$ of APC-doped cuprates and Fe-based superconducting films. If both these characteristic lengths can be changed, in addition to the enhancement in the flux pinning, $J_d$ can be dramatically improved through the enhancement in $J_d$. Increasing $T_c$ has been the empirical method for increasing $J_d$; however, this depends on discovering new superconductors, and even in the cases where this has been achieved (e.g., HgBa$_2$Ca$_2$Cu$_3$O$_{6+\delta}$ and Bi$_2$Sr$_2$Ca$_2$Cu$_3$O$_{10+\delta}$), it has not led to improved performance, as the gains have been negated by the enhancement in thermal fluctuations that grow, since

$$G_i^{1/2} \propto \left(\frac{\xi^2}{\lambda^2}\right)^{1/2}$$

(3)

where $G_i$ is the Ginzburg number.

Herein, we present a novel route for improving the performance of superconductors by increasing $J_d$. Unlike the increase in pinning, which is extrinsic, this route is thermodynamic: $J_d$ is raised by decreasing $\lambda$ and/or increasing $H_c \propto (\lambda\xi)^{-1}$. This method is general and applicable to any superconductor; herein, we show results for RE123 and Ba122:P films both with and without incoherent BZO NPs. The method works in conjunction with any pinning landscape improvement that has already been achieved, facilitating a method for increasing performance independent from the microstructure. As a concomitant advantage, the decrease in $\lambda$ also reduces the deleterious effects of thermal fluctuations by reducing $G_i$. In the RE123 compounds, we achieve this by increasing the carrier concentration, and thus decreasing $\lambda$; we also detect an increase in $H_c$ and a decrease in $y$ observed through the increased $H_{c2}$ (i.e., decrease in $\xi$) with a consequent reduction in $y$. When we combine this new strategy with our previously developed methods to incorporate a large density $N_{np}$ of incoherent BHO NPs of a tailored size, we obtain $J_c \sim 150$ MA/cm$^2$ (~32.4% of $J_d$) and $J_c \sim 130$ MA/cm$^2$ (~28% of $J_d$) at 4.2 K and self-field for nanocomposite (Y,Gd)123 films on single-crystal substrates and metallic substrates (coated conductors), respectively. These improvements carry over to the in-field properties. We also apply this route in Ba122:P films with incoherent BZO NPs, where we can increase $J_d$ and $J_c$ by controlling $\lambda$ and $\xi$ through the tuning of the chemical pressure. This coordinated strategy can inform the improvement efforts in the newly discovered hydrogen-based superconductors.

We start by increasing $J_d$ by decreasing $\lambda$ and $\xi$ for RE123. The Cu-O planes containing chains in RE123 are an exception among other cuprates (La$_{2-x}$Sr$_x$CuO$_4$), Y$_{1-x}$Cu$_x$Sr$_2$Cu$_3$Te$_{1-y}$Pb$_y$O$_{6+y}$, Tl$_2$Ba$_2$CuO$_{6+y}$ or Fe-pnictides. This allows a unique opportunity for $\lambda$ to be decreased and $H_c$ to be increased up to the highest possible overdoping, unlike other cuprates and Fe-pnictides, for which $\lambda$ is minimized at the optimum $T_c$.

An indication of the possible gain in terms of enhancing $J_d$ by tuning the carrier concentration is observed in the specific heat jump (directly related to $H_c$) that for $y = 7$ ($p = 0.19$) is 45% higher than for optimum doping. These beneficial effects outweigh the negative effects of the 4% decrease in $T_c$. Thus, we proceed to
change the oxygen content $y$ and modify the carrier concentration $p$ to ultimately change $\lambda$ and $\xi$ for RE123 with two very different pinning landscapes. In Table 1, we summarize the main experimental results for the RE123 compounds. To avoid changes stemming from different $T_c$ values, we compare two samples with similar $T_c$ (89.2 and 90.2 K) that are on either side of the optimal doping, i.e., $p = 0.18$ and 0.144. A comparison of these samples leads to $J_d$ values of 498 and 230 MA/cm$^2$, respectively, almost an increase by a factor of two with decreases in $\lambda$ and $\xi$.

### Materials and methods

#### Film growth

The epitaxially grown Y123 nanocomposite films of standard (Y,Gd)123 and BHO NP-doped (Y,Gd)123 ((Y,Gd)123 + BHO) films were grown from metal organic solutions including Y-, Gd-, and Ba-trifluoroacetates and Cu-naphthenate with a cation ratio of 0.77:0.23:1.5:3 on buffered tapes of CeO$_2$ (grain-boundary angles, $\Delta \phi_{CeO_2} = 3.0^\circ$)/Y$_2$O$_3$/LaMnO$_3$/ion-beam-assisted deposition (IBAD)-MgO/Gd$_2$Zr$_2$O$_7$/Hastelloy C276 (Haynes International Inc., Kokomo, IN, USA). We added HF-naphthenate into the (Y,Gd)123 solutions; the volume percent of BHO was 12, and the concentration of the naphthenate into the (Y,Gd)123 solutions including Y-, Gd-, and Ba-tri-naphthenate was 1.5:3 mol. % BaZrO$_3$ (BZO)-doped epitaxial films were deposited on MgO (100) single-crystal substrates by ablating the polycrystalline pulsed laser deposition targets using the second harmonic (wavelength: 532 nm) of a pulsed Nd:YAG laser at a repetition rate of 10 Hz in a vacuum of $10^{-5}$ Pa at a substrate temperature of 850°C. In this work, the amount of P substitution $x$ in the target was selected as 0.33, 0.40, and 0.50. The total thickness of the (Ba122-P) films with and without BZO was 80 nm.

#### Oxygenation treatments for cuprate films

The oxygenation treatments were precisely controlled to tune the carrier concentration for the (Y,Gd)123 + BHO coated conductors (CCs). The oxygenation process is reversible, as confirmed by the ability to recover $T_{c,zero}$ and $J_d$ after varying the oxygen content $y$. The optimal dopingannealing temperature ($T_{opt}$) was found to depend on the RE element. For maximum $T_c$, RE123 with larger RE$^{3+}$ ions required lower O$_2$ annealing temperatures compared to RE123 with smaller RE$^{3+}$ ions (at the same O$_2$ pressure). $T_{opt}$ (the temperature for the highest $T_{c,zero}$ and smallest $\Delta T (= T_{canon} - T_{c,zero}$ for each RE123 material) for our RE123 CCs prepared by different growth methods (MOD and PLD) is consistent with that of bulk studies, at $T_{opt} = 500, 450$ and 350°C for Y123, (Y,Gd)123 and Eu123 CCs, respectively. In this work, for the oxygenation of the RE123 films prepared from different fabrication processes (MOD and PLD), we annealed in an O$_2$ environment of 1.1 atm, and each annealing temperature ($T_A = 300–550 ^\circ C$) was held for 3 h and then rapidly quenched to room temperature. From the $c$-axis length...
measured by XRD (RINT2100 and ATX-G (Rigaku Co., Tokyo, Japan)) and $T_{c,\text{zero}}$ annealing at 300 °C for 3 h was sufficient to oxygenate the RE123 films.

**Transport properties in magnetic fields**

The films were patterned using a pulsed fiber laser (1095 nm, 20 W) into bridges of ~50 µm width. The crystalline quality was examined by X-ray diffraction (XRD). The temperature dependence of the resistivity ($\rho$) was measured by a four-probe method in the temperature range of 4–300 K using a physical property measurement system (PPMS, Quantum Design, Inc., San Diego, CA, USA) with a superconducting magnet generating a field H up to 14 T and in an 18 T-superconducting magnet at Tohoku University. In the PPMS, a rotational stage was used to rotate the samples with respect to H. The critical current was determined using a 1 µV cm$^{-1}$ criterion. $H_{c2}$ and $H_{cr}$ were determined using 0.90 $\rho_N$ and 0.01$\rho_N$ criteria, respectively, where $\rho_N$ is the normal-state resistivity. Hall measurements were performed using a SQUID (Quantum Design, Inc., San Diego, CA, USA) magnetometer to characterize the temperature and field dependence of $J_c$ and $S$.

**Results**

**Controlling the carrier density of the superconducting films**

First, to investigate the effects of introducing coherent BHO nanorods on the $T_{c,\text{zero}}$ c-axis length and self-field $J_c$ ($J_{c,s.f.}$), we measured the hole concentration ($n_{d1}$, determined from the Hall effect at 300 K) dependence of these properties for both standard Eu123 and Eu123 with coherent BHO nanorod (Eu123 + coherent BHO) CCs grown by PLD (Fig. 1a, b). $T_{c,\text{zero}}$ is determined using a 0.01$\rho_N$ criterion. As shown in the inset of Fig. 1a, the Eu123 + coherent BHO CC has coherent BHO nanorods with a diameter of 5 nm. As shown in Fig. 1a, the $T_{c,\text{zero}}$ and c-axis length of the standard Eu123 CCs decrease systematically with decreasing oxygenation temperature ($T_A$) from $n_{d1}^{300K} = 9.4 \times 10^{21}$/cm$^3$ (optimum doped) to $15.3 \times 10^{21}$/cm$^3$, confirming that the samples are in the overdoped regime. On the other hand, although the Eu123 + coherent BHO CCs are treated under the same $O_2$ annealing conditions as the overdoped standard CCs, $T_{c,\text{zero}}$ is not reached even for the optimum doping level (i.e., underdoped regime), and the c-axis length is longer than that in standard Eu123 CCs. Figure 1b shows $J_{c,s.f.}$ as a function of carrier concentration (doping level) in the CuO$_2$ layer ($p$) for both the standard Eu123 and Eu123 + coherent BHO CCs. The variation in $p$ is determined by following $T_{c,\text{zero}}$ on the universal doping curve$^{29}$, where $T_{c,\text{zero}}$ reaches its maximum at optimum doping ($p = 0.16$) (see Supplementary Information, Fig. S3). As a result, although the Eu123 + coherent BHO films have strong pinning, the $J_{c,s.f.}$ of the nanocomposite CCs is not enhanced compared to that of the standard ones because the carrier concentration $p$ is lower due to the strain-induced oxygen-vacancy formation, leading to a reduction in the carrier doping level$^7$. There are no reports of overdoped RE123 with coherent APCs because it is generally difficult to overdope coherent APC-doped RE123 films, although overdoping is easily achieved in standard films (with no APCs).

Now, we focus on our incoherent BHO NP-doped (Y,Gd)123 CCs. As shown in Fig. 1c, although the (Y,Gd)123 + BHO CCs have a high density of NPs (see inset of Fig. 1c), $T_{c,\text{zero}}$ and the c-axis length systematically decrease with decreasing oxygenation temperature ($T_A$) from $n_{d1}^{300K} = 9.4 \times 10^{21}$/cm$^3$ (optimum doped) to $21 \times 10^{21}$/cm$^3$, attaining overdoped status. However, the $J_{c,s.f.}$ at 77 K (see Fig. 1d) increases monotonically with increasing $p$ beyond optimum doping. Even though the (Y,Gd)123 and (Y,Gd)123 + BHO CCs have almost the same $T_{c,\text{zero}}$–$n_{d1}$ broad peak (because the superconducting matrix remains intact$^{11}$), the $J_{c,s.f.}$ of the (Y,Gd)123 + BHO CC is over two times higher than that of the (Y,Gd)123 CC. It is worth noting that even though $T_{c,\text{zero}} \sim 90$ K is almost the same for the (Y,Gd)123 + BHO CCs with $n_{d1}^{300K} = 7 \times 10^{21}$/cm$^3$ and $n_{d1}^{300K} = 21 \times 10^{21}$/cm$^3$, as shown in Fig. 1c, the overdoped CC shows a $J_{c,s.f.}$ 1.8 times higher at 77 K. It is worth noting that we achieved an overdoped doping level up to $p = 0.18$ for our incoherent BHO NP-doped (Y,Gd)123 CCs but not for the standard one (without APCs).

**Influence of grain boundaries in carrier density-controlled films**

To clarify that the enhancement in $J_c$ (Fig. 1d) for our overdoped (Y,Gd)123 + BHO CCs, which are fabricated on oxide-buffered metallic substrates (in-plane crystallinity ($\Delta \phi_{CeO_2} = 3^\circ$)), is not due to doping-induced improved grain-boundary properties (similar to the improvement in the intergrain-$J_c$ for Ca-doped Y123 films on bicrystal substrates$^{38}$), we investigated the in-plane crystallinity of CeO$_2$ ($\Delta \phi_{CeO_2}$) buffered metallic substrates with respect to the self-field $J_c$ at 77 K of overdoped (Y,Gd)123, underdoped (Y,Gd)123 + BaHfO$_3$ and overdoped (Y,Gd)123 + BaHfO$_3$ films (Fig. 2a). For $\Delta \phi_{CeO_2} > 3^\circ$, the $J_{c,s.f.}$ of all films decreases exponentially with increasing boundary angle. However, for $\Delta \phi_{CeO_2} < 3^\circ$, the $J_{c,s.f.}$ of all films decreases by just 10% when changing $\Delta \phi_{CeO_2}$ from 0.6° to 3° independent of $p$ and of the pinning landscape. As shown in Fig. 2b, although the ratio of $J_{c,s.f.}(\Delta \phi)/J_{c,s.f.}(0.6^\circ)$ for $\Delta \phi_{CeO_2} > 3^\circ$ of the two undoped films is lower than that of the overdoped film, the ratio for
Δψ_{CeO2} < 3° clearly shows exactly the same trend even for different p-values (underdoped and overdoped) and for different microstructures (without and with BHO NPs). To investigate the GB misorientation angles in our MOD CCs, we studied the plan-view TEM images of (Y,Gd)123 CCs on Δψ_{CeO2} = 3° buffered metallic substrates (see inset of Fig. 2b). The chain of edge dislocation distances (D) is 13.5–15.3 nm for a film on Δψ_{CeO2} = 3°, which represents the misorientation angles of 1.5–1.7° calculated using $D = (|b|/2)/\sin(\theta_{GB}/2)$, where $|b|$ is the norm of the corresponding Burgers vector. Because the crystal growth of MOD films is meandering and passes over the substrate grain boundaries (differing from that in PLD), the value of the misorientation angle is almost half that of Δψ_{CeO2}, which is the same as the in-plane crystallinity of (Y,Gd)123 ($\Delta \phi_{(Y,Gd)123}(103) = 1.5^\circ$), as evaluated by XRD. It is clear that the GBs of (Y,Gd)123 and (Y,Gd)123 + BaHfO3 CCs grown on Δψ_{CeO2} = 3° of CeO2 buffered metallic substrates are not Josephson weakly linked (i.e., with a locally suppressed order parameter). Based on Fig. 2a, b, we conclude that our $J_c$ properties for films grown on Δψ_{CeO2} = 3° of CeO2 buffered metallic substrates mainly depend on the value of the intragrain $J_c$, not the intergrain-$J_c$ as is the case for large misorientation angles of the GBs30.

**Penetration depth and coherence length in carrier-controlled films**

In Fig. 3, we show that $\lambda$ and $\xi$ vary with carrier concentration (p). We observed changes consistent with those found in the literature for single-crystal samples. The upper panel of Fig. 3a presents the measured $\lambda_{ab}$ as a
function of $p$ for Y123,$^{23,31}$ and (Y,Ca)123$^{32}$ single-crystals. For refs. $^{23,31}$, we calculated the penetration depth using $\lambda_{ab} = [|\lambda_{ab}|]^{1/2}$. For the extraction of $\lambda_{ab}(0)$ for our (Y,Gd)123 + BHO film, we use the temperature dependence of the resonant frequency of the coplanar waveguide resonators based on the equations derived by K. Watanabe et al.$^{33}$ (measurement details are shown in SI, Figs. S4 and S5). Indeed, for $\lambda_{ab}(0)$, the decrease with increasing $p$ for (Y,Gd)123 + BHO films is similar to that of Y123 and (Y,Ca)123 single-crystals$^{23,31,32}$.

The $H_{c2}(0)$ for $H||c$ for the (Y,Gd)123 + BHO CCs with different $p$-values are shown in the lower panel of Fig. 3a. The values for (Y,Gd)123 + BHO CCs and Gd123 single-crystals are estimated by using the Werthamer–Helfand–Hohenberg (WHH) formula$^{34}$ (detailed data in SI, Figs. S6 and S7). The (Y,Gd)123 + BHO CCs with $p = 0.144, 0.168$ and 0.180 exhibit an upward trend in $H_{c2}(0)$ similar to that of Gd123 single-crystals (measured) and Y123 single-crystals from ref. $^{35}$. The $\mu_0H_{c2}^0(0)$ vs. $p$ trend for our (Y,Gd)123 + BHO CCs and the Gd123 single-crystal is consistent with Y123 single-crystal studies, showing that $H_{c2}$ increases with $p$ up to $p = 0.18$.

Using $\lambda_{ab}$ (upper panel of Fig. 3a) and $\xi_{ab}$, we calculated $H_{c2}(0)$ using $\mu_0H_{c2}^0(0) = \frac{2\pi\lambda_{ab}(0)\xi_{ab}(0)}{\Delta_0}$ for our (Y,Gd)123 + BHO films and Y123 single-crystals$^{23,31,35}$ with various $p$-values, as shown in the upper panel of Fig. 3b. These results are consistent with the calculated $H_{c2}(0)$ values based on $H_{c2}$ and $H_{c1}$ for the Gd123 single-crystal (detailed data in SI, Fig. S7). The $H_{c2}(0)$ values for the (Y,Gd)123 + BHO CCs increase with increasing $p$, which is a similar trend to that for the Gd123 and Y123 single-crystals.

In view of the changes in $\xi$ and $\lambda$, summarized in Table 1, we can use $J_d \propto \left(\frac{1}{\xi^2}\right)$ and assert that the variation in $\lambda$ is more important for $J_d$ than the variation in $\xi$, as $\lambda$ also affects $H_{c2}$. The enhanced $H_{c2}$ is one of the main reasons for the higher $J_c$ of our most overdoped (Y,Gd)123 + BHO film with $p = 0.18$ and the $J_c$ calculated for strong pinning nanoparticle-doped films, $J_c^{\text{NPd}} \propto \left(\frac{1}{\xi^2}\right)$ (see Supplementary Information, Section 9). The monotonic increase in $H_{c2}(0)$ with $p$ shown in the upper panel of Fig. 3b, consistent with previous studies in single-crystal$^{36}$ and polycrystalline$^{37}$ Y123, confirms the different behavior of Y123 compared to other HTS cuprate materials where $H_{c2}(0)$ and $\Delta C/T_c$ coincide with the maximum of $T_c$.$^{20,22}$

To investigate the $n_s$ dependence of the normal-state carrier density for Y123, we calculated $n_s$ for (Y,Gd)123 + BHO CCs with different $p$. The dependence of the effective mass ($m^*$) in Y123 single-crystals on the hole doping level was recently measured$^{37}$. To calculate the $n_s$ for our (Y,Gd)123 + BHO CCs, we used the relationship $\lambda_{ab}(0) = \sqrt{\frac{m^*}{m_{ab}(0)}}$ and $m^*$ from reference$^{37}$ (no $m^*$ data above $p = 0.152$ was reported, so we extrapolated from the available curve). The $n_s$ for our (Y,Gd)123 + BHO CCs increases monotonically with the hole concentration, as shown in the lower panel of Fig. 3b. This is consistent with the Y123 single-crystal data, also shown for comparison$^{23,31}$.

As shown in Fig. 3, the overdoped (Y,Gd)123 + BHO CCs have larger $H_{c2}$ and smaller $\lambda_{ab}$ than the under—and optimally doped CCs, indicating an increase with $p$ of $J_c$ ($\propto \lambda^{-2}\xi$) and $J_d$ ($\propto c\lambda^{-2}\xi^{-1}$). From Formula (1), the
(Y,Gd)\textsubscript{123} + BHO CCs with $p = 0.144$, 0.168 and 0.180 yield $J_d(0) = 230$, 368 and 498 MA/cm\textsuperscript{2}, respectively. This remarkable enhancement in the $J_d(0)$ of the overdoped sample is due to the reduced $\xi_{ab}(0)$ and $\lambda_{ab}(0)$ achieved by controlling the carrier density.

**Substantially higher $J_c$ at all temperatures**

Consistent with the enhancements in $J_d$ being induced by the changes in $\lambda_{ab}$, we observed the same enhancement at all temperatures over a wide range of applied magnetic fields. The upper panel of Fig. 4a shows the calculated $J_d(T)$ with different $p$ based on the parameters in Table 1. The overdoped (Y,Gd)\textsubscript{123} + BHO CC ($p = 0.18$) has a higher $J_d(T)$ than films with $p = 0.168$ and 0.144. As seen in the lower panel of Fig. 4a, the $J_d(T)$ for $p = 0.18$ is ~2 times higher than that for $p = 0.144$ over a wide temperature range. Figure 4b shows $J_c^{s.f.}(T)$ for the (Y,Gd)\textsubscript{123} + BHO CCs with different $p$. Even though all the CCs have the same high density of BHO nanoparticles, $J_c^{s.f.}$ for $p = 0.18$ is the highest at all temperatures. Although CCs with $p = 0.18$ and $p = 0.144$ have almost the same $T_c$, slightly lower than that for the optimum doped one, the $J_c^{s.f.}$ of the $p = 0.18$ film is almost twice that of $p = 0.144$. At $p = 0.18$, the $J_c^{s.f.}$ for the (Y,Gd)\textsubscript{123} + BHO CC achieves a maximum value of 130 MA/cm\textsuperscript{2} at 4.2 K. This is higher than that previously reported for any superconducting material except nanowires and ultrathin films (where the flux pinning mechanism is different). The $J_c^{s.f.}$ results are independent of the sample’s width ($W$) and length ($L$), as demonstrated by the results at 77 K (SI, Fig. S8), indicating very uniform superconducting films.
the same enhancement of 1.1 at 77 K (compared to the $J_{c,s.f.}$ of films on $\Delta \phi_{eoor} = 1^\circ$ and $\Delta \phi_{ceoc2} = 1^\circ$ of substrates in Fig. 2b) due to the slightly higher in-plane crystallinity of the former.

Insights into the benefit of further controlling $J_d$ by changing the hole doping level are given by the in-field $J_{c}(T)$ at $\mu_0 H = 0.3$ T and $H||c$ in Fig. 4c. The overdoped $(Y,Gd)123+BHO$ CC ($p = 0.18$) shows the highest in-field $J_c$, approximately twice the value for $p = 0.145$. As shown in the inset of Fig. 4c, the transport $J_c$ coincides very well with the $J_c$ calculated from magnetization using the Bean model$^{42}$, indicating that our $J_c$ values are highly uniform and reproducible. The solid lines in the upper panel of Fig. 4c are the calculated $J_c(J_{0,cal}^{NPX})$ and the solid symbols are the experimentally obtained parameters (calculation details are shown in Supplementary Information, Table S2), indicating that $J_{0,cal}^{NPX}$ for $(Y,Gd)123+BHO$ CCs with different $p$ are in good agreement with the experimental $J_c$. This agreement confirms the critical role of the decrease in $\lambda$ and increase in $H_c$. The most interesting and important feature of the data presented here is that the enhancement ratios in $J_d-T$ and $J_c-T$ in both the self and in-field are identical (see lower panels of Fig. 4). This confirms that we can enhance $J_c$ by enhancing $J_d$ by changing $H_c$ and $\lambda$ while keeping the pinning enhancement intact.

Ginzburg number of carrier-controlled films

The top panel of Fig. 5a shows the $\gamma$ values for $(Y,Gd)123$ and $(Y, Gd)123+BHO$ CCs with various hole concentrations measured at 300 K. The $\gamma$ is calculated from the angular dependence of $H_{c2}$ (see Supplementary Information, Fig. S9 and ref. 43 for details). For CCs both with and without BHO, the $c$-axis length (Fig. 1c) and mass anisotropy decrease with increasing $n_H$, i.e., hole doping level. These dependences follow the same trend observed in the $c$-axis length vs. $p$ characteristics of the $Y_{123}$ SC$^{44}$ and in the $\gamma$ vs. $p$ characteristics of the $(Y, Ca)$ 123 SC$^{45}$. We also observed a systematic reduction in the $c$-axis length and smaller mass anisotropy for the samples with nanoparticles. The origin of this effect is under investigation and will be the focus of future publications.

As indicated above, the reduction in $\gamma$ also diminishes the effect of thermal fluctuations, as characterized by $G_t \sim \gamma^{-2}$ (see Formula (3)). While $J_c$ increases by increasing $J_d$, it can also increase by reducing the effect of flux creep. The effect of flux creep is characterized by the creep rate, $S$, with which pinned vortices escape from the pinning
centers under thermal agitation. It was found that there is a universal lower limit of the creep rate $S_{\text{min}} \sim G^{1/2}(T/T_c)^{18}$, which demonstrates that the creep rate can be essentially reduced by reducing the anisotropy of the superconductor. In addition, $S$ can also be reduced to its limit $S_{\text{min}}$ by adding pinning.

The bottom panel of Fig. 5a shows $S(T=50\, K, \mu_0H=0.3\, T) \text{ vs. } n_{H}$ for our CCs, as a representative example of $S(T,H)$ over a wide range of conditions outside the Anderson-Kim (A–K) regime. This relationship can also be replotted as that of $S(T=T_c/4, \mu_0H=1\, T)$ (i.e., inside the A–K regime) vs. $G^{1/2}$, as shown in Fig. 5b. Thus, reducing the anisotropy is a new way to reduce $S$. In addition, the introduction of nanoparticles is effective, as seen from the comparison between $(Y,Gd)_{123}+BHO$ CCs and $(Y,Gd)_{123}$ CCs.

**Discussion**

The effect of $J_d$ on $J_c$ is general and apparent for different superconductors with varied pinning landscapes (see Fig. 6). Herein, we display $J_c$ vs. $J_d$ at $4.2\, K$ \cite{53}. Details of the calculation parameters for $J_d$ and experimentally obtained $J_c$ are shown in SI, Table S3. First, we see that there is a general trend for several superconductors in which $J_c$ is proportional to $J_d$ (clearly seen in the inset of Fig. 6). Second, as shown in Fig. 6 for standard $(Y,Gd)_{123}$ CCs, we can tune $J_c$ at $4.2\, K$ from 23.5 to 44.5 MA/cm$^2$ by changing $J_d$. We note that the relation of $J_c \sim 0.1J_d$ remains unchanged. Enhancements in $J_d$ and $J_c$ by tuning the carrier concentration are also observed for Ca-doped Y123 SC \cite{50}. Third, the combination of controlling $J_d$ by tuning the carrier concentration in a film with a high density of nanoparticles leads to the highest $J_c$ at $4.2\, K = 130$ MA/cm$^2$ for $(Y,Gd)_{123}+BHO$ CCs, which is 28.0% $J_d$. Moreover, a $(Y,Gd)_{123}+BHO$ film on a single-crystal achieved 32.4% $J_d$ ($J_c$ at $4.2\, K = 150$ MA/cm$^2$) because of the further improvement obtained by the higher in-plane crystallinity. This value is close to the 33% achievement predicted by Gurevich \cite{53} for a superconductor with NP pinning centers similar to the actual conditions in our $(Y,Gd)_{123}+BHO$ films and CCs.

As shown in the inset of Fig. 6, increasing $J_d$ is an effective method for enhancing $J_c$ for not only Y123 cuprate CCs but also Fe-based pnictide Ba122:P films. In the Ba122:P system, the isovalent substitution of P for As induces chemical pressure, suppressing magnetism and inducing superconductivity, which is different from the effect of electron doping or hole doping \cite{54–56}. For standard Ba122:P films, by tuning $x$, the $J_c$ at $4.2\, K$ increases from 1.0 to 3.6 MA/cm$^2$ due to the increase in $J_d$ from 23 to 74 MA/cm$^2$. Moreover, Ba122:P + BZO films with different $x$ show that $J_c$ increases (up to 8 MA/cm$^2$ at $4.2\, K$) with increasing $J_d$, indicating that the combined approach of tuning $J_d$ and enhancing flux pinning (i.e., adding NPs) can also be used to improve the performance of superconductors of different families. In this case, $J_c \sim G^{1/2}$.
regard, it is important to note that although the method for controlling $J_d (H_c$ and $\lambda_{ab})$ is different for the cuprate and the pnictide (changing carrier concentration ($p$) and the chemical pressure ($x$), respectively), the end result is the same, thus highlighting the general applicability of our strategy.

Further insight into the effects of the combination of increasing $J_d$ and enhancing flux pinning can be obtained from the field dependence of $J_c$. Figure 7a shows the $J_c(H||c)$ at 4.2 K for our overdoped (Y,Gd)123 + BHO CC compared with that of several RE123 films and CCs. As seen for up to 18 T, the $J_c(H||c)$ of overdoped (Y,Gd)123 + BHO CC is the highest among all superconductors. Compared with overdoped standard Y123 at 5 K, the $J_c(H||c)$ of overdoped (Y,Gd)123 + BHO CC is 144% at the self-field and 199% at 5 T. Moreover, compared to that of coherent BHO-doped CCs, the $J_c(H||c)$ of our CC shows a 254% increase at 1 T and 175% increase at 18 T. The remarkable in-field performance of overdoped (Y,Gd)123 + BHO CC is highlighted in Fig. 7b, where the pinning force, $F_p = J_c(H) \times \mu_0 H$, is compared with that of several RE123 materials. The $F_p$ at 4.2 K of our overdoped (Y,Gd)123 + BHO CC reaches ~3.17 TN/m³ at 18 T ($H||c$), which is the highest reported value for any superconductor material. Please note that because the anisotropy of RE123 materials is ~5 (Fig. 5a), the $F_p$ measured along the $c$ axis is the minimum value for a RE123 superconductor.

Conclusions

In summary, we have succeeded in combining this thermodynamic route (increasing $J_d$ by decreasing $\lambda$ and/or increasing $H_c$) with our previously developed methods to tailor the size and incorporate large densities of incoherent nanoparticles. We obtain $J_c \sim 150$ MA/cm² (~32.4% of $J_d$) and $J_c \sim 130$ MA/cm² (~28.0% of $J_d$) at 4.2 K and in the self-field for nanocomposite RE123 films on single-crystal substrates and metallic substrates (CCs), respectively. Moreover, for films of chemical-pressure-controlled Ba122:P with incoherent BZO NPs, the $J_c$ at 4.2 K increases from 1.0 to 8.0 MA/cm² due to the increase in $J_d$ in combination with the introduction of high densities of incoherent BZO NPs. To our knowledge, the $J_c$ values attained for our CC of overdoped (Y,Gd)123 in not only the self-field but also the high field are the highest reported to date for any superconductor. This highlights that thermodynamic improvements of superconductors can work in parallel with already successful artificial pinning centers and that a maximum $J_c \sim 0.3 J_d$ appears to be the current upper limit for the enhancement in $J_c$. 

Fig. 6 Self-field critical current density $J_{c,s.f.}$ v.s. depairing current density $J_d$ for various superconducting materials. $J_{c,s.f.}$ at 4.2 K as a function of $J_d$ at 4.2 K for different superconductors with varied pinning landscapes. Open and solid symbols indicate the $J_c$ for pristine and superconductors with introduced pinning centers. The inset of Fig. 6 shows $J_c$ vs. $J_d$ for chemical–pressure-controlled Fe-based pnictide Ba122:P films with and without nanoparticles.
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Author details
1Graduate School of Science and Technology, Seikei University, 3-3-1 Kichijoji-kitamachi, Musashino-shi, Tokyo 180-8633, Japan. 2Materials Physics and Applications Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA. 3JST-FOREST, 7, Gobancho, Chiyoda-ku, Tokyo 102-0076, Japan. 4Department of Basic Science, The University of Tokyo, Meguro, Tokyo 153-8902, Japan. 5Department of Electrical and Electronic Engineering, University of Yamanashi, 4-3-11 Takeda, Kofu 400-8511, Japan. 6Department of Applied Physics, The University of Tokyo, Bunkyo, Tokyo 113-8656, Japan.

Author contributions
M.M. and B.M. carried out the experimental design. M.M., G.T., and T.H. grew the films and carried out transport measurements. B.M. carried out the data analysis and provided advice and consultation on the flux pinning and manuscript preparation. R.Y. and T.K. carried out microstructural studies. Y.K. carried out the analysis for $H_B$. T.I. contributed to the discussion on the film preparation. H.K., F.N., and A.M. contributed to the discussion on the penetration depth analysis. K.S. and N.S. carried out the analysis for the resonance frequency. T.O. and S.A. contributed to the discussion on the analysis for the transport measurement at high field. L.C. contributed to the discussion and manuscript preparation. All authors discussed the results and implications and commented on the manuscript. M.M. and B.M. wrote the manuscript with contributions from all the authors.

Competing interests
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Fig. 7 Critical current density $J_c$ and pinning force $F_p$ as a function of magnetic field $H$. a $J_c(H)$ at 4.2 K and b $F_p(H)$ curve of overdoped (Y,Gd)123 + BHO CCs at 4.2 K and $H$. For comparison, the data for Sm123 + coheret BHO film$^{57}$, (Y,Gd)123 + coherent BZO CC$^{39}$, (Y,Gd)123 + coherent BHO CC$^{39}$, overdoped Y123 film at 5 K$^{16}$, and Y123 CCs$^{38}$ are included.
