Giant frictional drag in strongly interacting bilayers near filling factor one

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We study the frictional drag in high mobility, strongly interacting GaAs bilayer hole systems in the vicinity of the filling factor $\nu = 1$ quantum Hall state (QHS), at the same fillings where the bilayer resistivity displays a reentrant insulating phase. Our measurements reveal a very large longitudinal drag resistivity ($\rho_{xx}^D$) in this regime, exceeding 15 k$\Omega$/\square at filling factor $\nu = 1.15$. $\rho_{xx}^D$ shows a weak temperature dependence and appears to saturate at a finite, large value at the lowest temperatures. Our observations are consistent with theoretical models positing a phase separation, e.g. puddles of $\nu = 1$ QHS embedded in a different state, when the system makes a transition from the coherent $\nu = 1$ QHS to the weakly coupled $\nu = 2$ QHS.

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Closely spaced bilayer carrier systems have been the test ground for a multitude of novel electronic states with no counterpart in the single-layer case. The most important are quantum Hall states (QHSs) possessing interlayer coherence [1] at total filling factor $\nu = 1/2$ (layer filling $\nu_{\text{layer}} = 1/4$) [2, 3] and $\nu = 1$ ($\nu_{\text{layer}} = 1/2$) [4, 5]. These QHSs are stabilized when the interaction between carriers in the same layer is comparable to that of carriers residing in opposite layers. The $\nu = 1$ QHS has been shown to exhibit enhanced inter-layer tunnelling [6] reminiscent of a Josephson junction, as well as a peculiar, charge-neutral superfluid in counterflow transport [7, 8]. In a simple picture the $\nu = 1$ QHS can be regarded as a condensate of excitons [9], where carriers and vacancies pair-up in the opposite, half-filled layer forming excitons, which condense at lowest temperatures.

An equally interesting ground state also explored in conjunction with the emergence of high quality, interacting bilayer systems is the Wigner crystal (WC) [10]. Experimentally, transport measurements in electron and hole bilayers show a suppression of QHSs beyond a given filling factor, namely $\nu = 1/2$ in interacting electron bilayers [11] and $\nu = 1$ in interacting hole bilayers [12]. This observation is similar to the suppression of fully developed QHSs in single layers beyond $\nu = 1/5$ for electrons, and $\nu = 1/3$ for dilute holes which has been interpreted as a signature of the WC being stabilized at sufficiently low fillings [10]. Furthermore, the quenching of QHSs at sufficiently low fillings is accompanied by the existence of a reentrant insulating phase (RIP) around the lowest filling QHS, suggesting an onset of the WC state. In order to gain further insight into the physics of the RIP, here we study the frictional drag in interacting GaAs hole bilayers in the vicinity of the phase coherent $\nu = 1$ QHS, in the same filling factor range where the bilayer resistivity exhibits a RIP. Our results show an anomalously, record large longitudinal drag resistivity ($\rho_{xx}^D$) on the flanks of $\nu = 1$, larger than 15 k$\Omega$/\square. Equally anomalous is the relatively weak temperature dependence of $\rho_{xx}^D$; it follows a power law $\rho_{xx}^D \sim T^\alpha$, with $\alpha < 1$, and saturates at a finite value at the lowest temperatures.

Our sample is a Si-modulation-doped GaAs double-layer hole system grown on GaAs (311)A substrate. It consists of two GaAs quantum wells which have a width of 150 Å each and are separated by a 75 Å wide AlAs barrier. The sample is patterned in a Hall bar geometry of 100 μm width, aligned along the [01\bar{1}] crystal direction [13]. Diffused InZn ohmic contacts are placed at the end of each lead. We use a combination of front and back gates [14] to selectively deplete one of the layers near each contact. As grown, the densities in the two layers were $p_{T} = 2.6 \times 10^{10}$ cm$^{-2}$ and $p_B = 3.2 \times 10^{10}$ cm$^{-2}$ for the top and bottom layers, respectively. The mobility along [01\bar{1}] at these densities is approximately 200,000 cm$^2$/Vs. Metallic top and bottom gates are added on the active area to control the densities in the layers. The measurements are performed down to a temperature of $T = 30$ mK, and using standard low-current (0.5 nA-1 nA), low-frequency lock-in techniques.

Two types of measurement configurations are used in our study. In one (bilayer) configuration, current is passed through both top and bottom layers and the ohmic contacts connect both layers simultaneously. The voltage drops along and across the Hall bar, divided by the total bilayer current, represent the longitudinal ($\rho_{xx}^B$) and Hall ($\rho_{xB}^B$) bilayer resistivities. In a second (drag) configuration, current is passed in one (drive) layer only, by using the selective depletion technique around the ohmic contacts such that they connect to a single layer only [14]. The voltage drops measured in the opposite (drag) layer, divided by the drive current, represent the longitudinal ($\rho_{xx}^D$) and Hall ($\rho_{xB}^D$) drag resistivities. The drag resistivity provides a measure of the electron-electron scattering rate between the carriers in the drive layer and those in the drag layer. For the data presented here we adopt the following sign convention: the longitudinal (Hall) drag resistivity is defined as positive when...
FIG. 1: Bilayer and longitudinal drag resistivities (\(\rho_{xx}^B\) and \(\rho_{xx}^D\)) measured at \(T = 30\,\text{mK}\) for a balanced bilayer with \(p_{tot} = 5.5 \times 10^{10}\,\text{cm}^{-2}\). Note that both traces are plotted on the same scale. The inset shows the temperature dependence of \(\rho_{xx}^B\) data.

the voltage drop along (across) the drag layer is opposite to the voltage drop along (across) the drive layer. We performed the usual consistency checks associated with drag measurements \[9\]. Owing to the proximity of the two layers in our sample, there is a small but finite interlayer leakage current. This leakage translates into an uncertainty in frictional drag measurements, which does not exceed \(\pm 6\%\) in our study.

In the main panel of Fig. 1 we show \(\rho_{xx}^B\) and \(\rho_{xx}^D\) vs the applied perpendicular magnetic field (\(B\)), both measured at \(T = 30\,\text{mK}\). The total bilayer density is \(p_{tot} = 5.5 \times 10^{10}\,\text{cm}^{-2}\), equally distributed between the two layers (balanced). The data show a fully developed QHS at \(\nu = 1\), stabilized here solely by interlayer coherence \[10\]. In a simple picture the emergence of a QHS at \(\nu = 1\) can be understood by considering the pairing of carriers and vacancies in the opposite layers. At total filling factor one each layer has the lowest Landau level half full, i.e. has an equal number of carriers and vacancies. Owing to the close proximity of the two layers and the ensuing inter-layer interaction, it is energetically favorable to form carrier-vacancy pairs in the opposite layers, which condense at the lowest temperature. A spectacular signature of this phenomenon is the emergence of a neutral superfluid, experimentally observed when equal and opposite currents are passed in the two layers \[7\] \[8\]. The ratio between the interaction energy of carriers in different layers and in the same layer is commonly quantified by \(d/l_B\), where \(d\) is the interlayer distance and \(l_B = \sqrt{\hbar/eB}\) is the magnetic length at \(\nu = 1\). For the case examined in Fig. 1 this ratio is 1.33.

The inset of Fig. 1 shows \(\rho_{xx}^B\) measured at different temperatures, for the same layer densities as in the main panel. These data show that as the temperature is reduced a RIP develops on the flanks of the \(\nu = 1\) QHS. Most interestingly, the data of Fig. 1 show a very large longitudinal drag on the left flank of \(\nu = 1\), in the same filling factor range where \(\rho_{xx}^B\) exhibits a RIP. In contrast to typical drag measurements where the drag resistivity is one to three orders of magnitude smaller than the single layer resistance \[15\], Fig. 1 data reveal that \(\rho_{xx}^B\) and \(\rho_{xx}^D\) are of the same order or magnitude, which testifies to the strong interlayer coupling at these filling factors. Clearly frictional drag constitutes a substantial component of the longitudinal resistivity here, in contrast to frictional drag at \(B = 0\,\text{T}\) where drag is a very small perturbation.

In Fig. 2 we show \(\rho_{xx}^D\) (top panel) and \(\rho_{xy}^D\) (bottom panel) vs \(B\), measured at different temperatures ranging from 30mK to 630mK, and at the same layer densities as the data of Fig. 1. At the lowest temperatures the data of Fig. 2 show a nearly vanishing \(\rho_{xx}^D\) at \(\nu = 1\) and \(\rho_{xy}^D\) quantized at \(\hbar/e^2 = 25.88\,\text{k}\Omega\) \[17\]. The temperature dependence of the Hall drag measured at around
\( \nu = 1 \) is relatively weak: as \( T \) is increased \( \rho_{xx}^D \) remains close to the quantized value for \( T \) as high as 500mK. The weak temperature dependence of \( \rho_{xy}^D \) at \( \nu = 1 \) is consistent with previous results in GaAs hole bilayers, which show a vanishing counterflow Hall resistivity for temperatures below 500mK \[8\] and indicates a strong pairing of the carriers and vacancies in opposite layers. Figure 2 data (top panel) substantiates our observation of an anomalously large drag in the vicinity of \( \nu = 1 \) QHS. As the temperature is increased \( \rho_{xx}^D \) increases, reaching a record 17k\Omega/\square at \( T = 630\text{mK} \) at \( \nu = 1.10 \). Equally noteworthy is that the onset of the anomalously large \( \rho_{xx}^D \) coincides with the onset of the non-zero \( \rho_{xy}^D \) indicating that the particle-vacancy pairing which stabilizes the \( \nu = 1 \) QHS is also responsible for the observed anomalously large \( \rho_{xx}^D \).

Next we present the temperature dependence of the anomalously large longitudinal drag observed near \( \nu = 1 \). Figure 3 shows the \( \rho_{xx}^D \) vs \( T \) data from 30mK to 630mK. An increase in interlayer current prevents an accurate measurement of the frictional drag near \( \nu = 1 \) above \( T = 700\text{mK} \). The \( \rho_{xx}^D \) data were measured in two different cooldowns at \( \nu = 1.10 \) and \( \nu = 1.15 \), namely fillings where the RIP reaches the maximum resistance. Note that \( \rho_{xx}^D \) maximum shifts slightly from \( \nu = 1.15 \) at the lowest \( T \) to \( \nu = 1.10 \) at the highest \( T \), as apparent from Fig. 2 (top panel) data. Several features of Fig. 3 data are noteworthy. First, \( \rho_{xx}^D \) exhibit a weak, slightly sublinear temperature dependence in the range \( T = 100 - 500\text{mK} \), which contrasts the more common \( \rho_{xx}^D \propto T^2 \) characteristic of the Coulomb drag in two-dimensional electron systems \[15\] or \( \rho_{xx}^D \propto T^{4/3} \) observed in drag measurements between composite fermions \[18\]. Second, \( \rho_{xx}^D \) appears to saturate at a constant, finite value below \( T = 100\text{mK} \) as \( T \) is increased.

![FIG. 3: Temperature dependence of \( \rho_{xx}^D \) measured at \( \nu = 1.10 \) and \( \nu = 1.15 \) in two different cooldowns. The different temperature dependences in separate cooldowns suggest that sample disorder affects the measured \( \rho_{xx}^D \).](image)

Third, the large \( \rho_{xx}^D \) near \( \nu = 1 \) shows a cooldown dependence, suggesting that sample disorder affects the measured \( \rho_{xx}^D \).

Before discussing our observation of enhanced frictional drag in the vicinity of \( \nu = 1 \) within existing theoretical models, we summarize the salient features of the experimental data. First, the longitudinal drag is greatly enhanced in the vicinity of the bilayer \( \nu = 1 \) QHS, exceeds 15 k\Omega/\square, and becomes comparable to the single-layer longitudinal resistivity. Second, the observed giant longitudinal drag emerges concomitantly with the large Hall drag near \( \nu = 1 \), indicating that particle-vacancy pairing is present. Third, the giant longitudinal drag has a weak, sub-linear temperature dependence, and appears to saturate at a finite, and large value (\( \geq 5k\Omega/\square \)) at the lowest temperatures. Finally, the frictional drag exhibits a cooldown dependence, which suggests that disorder affects the measured \( \rho_{xx}^D \) value. These features contrast the frictional drag between two two-dimensional carrier systems, which typically has a small (\( \leq 100\Omega \)) magnitude, and a \( \rho_{xx}^D \propto T^2 \) temperature dependence \[13\]. And while our measurements are performed in the quantum Hall regime where an agreement with Fermi liquid theory \[20\, 21\] should not be expected, these highlighted differences are nonetheless stark.

Our data can qualitatively be explained by theoretical models which invoke the coexistence of two phases as the system makes a transition, driven by filling factor in our case, from the \( \nu = 1 \) QHS to the weakly coupled \( \nu = 2 \) QHS. The \( \nu = 2 \) QHS consists of a pair of \( \nu_{\text{layer}} = 1 \)
QHSs, one in each of the two layers. Stern and Halperin \cite{22} examined theoretically the transition between the strongly coupled $\nu = 1$ QHS and two weakly coupled layers, each at $\nu_{\text{layer}} = 1/2$. By postulating that in the transition regime the system is composed of puddles of $\nu = 1$ QHS and two weakly coupled layers at $\nu = 1/2$ each on the other, they derive an expression for the longitudinal and Hall drag as a function of the fraction of the $\nu = 1$ QHS across the transition. Their model predicts a large longitudinal drag, as high as $h/2e^2$ in the transition regime, concomitantly with a non-zero Hall drag. Their results can be analytically be approximated by a simple semi-circle relation for the drag resistivity tensor,

$$ (\rho_{xx}^D + 1/2)^2 + (\rho_{xy}^D)^2 = 1/4 $$

with the resistivity expressed in units of $h/e^2$. Kellogg et al. \cite{23} have experimentally probed this transition by varying the total bilayer density, which in turn changes $d/l_B$. They observe an enhanced longitudinal drag in the transition region, in qualitative agreement with the theoretical model \cite{22}.

In order to quantitatively compare our experimental results with the model of Ref. 22, in Fig. 4 we show $\rho_{xx}^D$ vs $\rho_{xy}^D$ at different temperatures along with the semi-circle law of Eq. (1). The end points of the semi-circle, namely $\rho_{xx}^D = \rho_{xy}^D = 0$ and $\rho_{xx}^D = 0$, $\rho_{xy}^D = -1$, represent the weakly and strongly coupled bilayer regimes at $\nu \geq 2$ and $\nu = 1$, respectively. As the system makes the transition from weakly to strongly coupled, $\rho_{xx}^D$ and $\rho_{xy}^D$ depart from zero simultaneously, with $\rho_{xx}^D$ reaching a temperature dependent maximum. $\rho_{xx}^D$ is close to $h/2e^2 = 12.9$ kΩ/cm predicted by Eq. (1). At intermediate temperatures $T \approx 300$K the $\rho_{xx}^D$ vs $\rho_{xy}^D$ data are in very good quantitative agreement with the semi-circle law of Eq. (1), but depart from it at the lowest temperatures. We note however that Eq. (1) is expected to hold quantitatively if the drag resistivity is large compared to the symmetric (parallel flow) bilayer resistivity at all fillings, and also neglects the bilayer and drag resistivities in the weakly coupled regime. In light of these approximations, the agreement with the simple semi-circle law is satisfactory.

A separate model, also invoking the co-existence of two phases, that may explain the giant frictional drag data has been proposed by Spivak and Kivelson \cite{24}. The model of Ref. 24 considers the frictional drag between a passive layer and a low-density two-dimensional system where the ground state consists of bubbles of Wigner crystal (WC) embedded in a Fermi liquid. Each WC bubble in the active layer casts an image in the passive layer, which can be pictured as a hard wall potential being dragged in the passive layer. This in turn results in a significant scattering for the electrons in the passive layer, hence an anomalously large frictional drag. We speculate that one plausible scenario for the large drag in the vicinity of $\nu = 1$ in our sample is a "micro-emulsion" of the $\nu = 1$ QHS co-existing with a WC state.

In summary we report the observation of giant frictional drag in the vicinity of the strongly coupled bilayer $\nu = 1$ QHS. The giant longitudinal drag emerges concomitantly with a non-zero Hall drag, indicating the particle-vacancy pairing in this regime. Our observations are consistent with theoretical models \cite{22,23} which invoke the co-existence of two distinct phases as the system makes a transition from the $\nu = 1$ bilayer QHS, e.g. puddles of $\nu = 1$ QHS embedded in a weakly coupled bulk state or in a Wigner crystal state.

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\begin{thebibliography}{99}
\item[1] X.-G. Wen and A. Zee, Phys. Rev. Lett. 69, 1811 (1992).
\item[2] Y.-W. Suen et al., Phys. Rev. Lett. 68, 1379 (1992).
\item[3] J. P. Eisenstein et al., Phys. Rev. Lett. 68, 1383 (1992).
\item[4] S. Q. Murphy et al., Phys. Rev. Lett. 72, 728 (1994).
\item[5] T. S. Lay et al., Phys. Rev. B 50, 17725 (1994).
\item[6] I. B. Spielman et al., Phys. Rev. Lett. 84, 5808 (2000).
\item[7] M. Kellogg et al., Phys. Rev. Lett. 93, 036801 (2004).
\item[8] E. Tutuc, M. Shaveyan, D. A. Huse, Phys. Rev. Lett. 93, 036802 (2004).
\item[9] K. Yang et al., Phys. Rev. Lett. 72, 732 (1994); K. Moon et al., Phys. Rev. B 51, 5138 (1995).
\item[10] For a review of the WC state in two-dimensional systems, see M. Shaveyan, in Perspectives in Quantum Hall Effects, edited by S. Das Sarma and A. Pinczuk (Wiley, New York, 1997), p. 343.
\item[11] H.C. Manoharan et al., Phys. Rev. Lett. 77, 1813 (1996).
\item[12] E. Tutuc et al., Phys. Rev. Lett. 91, 076802 (2003).
\item[13] Hole systems grown on GaAs (311)A substrates exhibit a mobility anisotropy stemming from an anisotropic surface morphology, with the mobility being lower for current parallel to [011].
\item[14] J.P. Eisenstein et al., Appl. Phys. Lett. 57, 2324 (1990).
\item[15] T.J. Gramila et al., Phys. Rev. Lett. 66, 1216 (1991).
\item[16] The tunneling energy, i.e. the symmetrac-antisymmetric splitting, deduced from inter-layer tunneling measurements is $90 \mu$K for the bilayer system studied here; for more details see S. Misra et al., Phys. Rev. B 77, 161301(R) (2008).
\item[17] M. Kellogg et al., Phys. Rev. Lett. 88, 126804 (2002).
\item[18] M.P. Lilly et al., Phys. Rev. Lett. 80, 1714 (1998).
\item[19] While took precautions to use sufficiently low currents to avoid carrier Joule heating, we cannot rule out a lack of full carrier thermalization at the lowest temperatures.
\item[20] P. M. Price, Physica B 117, 750 (1983).
\item[21] L. Zheng and A. H. MacDonald, Phys. Rev. B 48, 8203 (1993).
\item[22] A. Stern and B. I. Halperin, Phys. Rev. Lett. 88, 106801 (2002).
\item[23] M. Kellogg et al., Phys. Rev. Lett. 88, 126804 (2002).
\item[24] B. Spivak and S. A. Kivelson, Phys. Rev. B 72, 045355 (2005).
\end{thebibliography}