Rapid Variability in the SOL2011-08-04 Flare: Implications for Electron Acceleration

Alexander T. Altyntsev1, Nataliia S. Meshalkina1, Alexandra L. Lysenko2 ©, and Gregory D. Fleishman3 ©

1 Institute of Solar-Terrestrial Physics, 126a Lermontov St., Irkutsk, 664033, Russia; nata@iszf.irk.ru
2 Ioffe Institute, Polytekhnicheskaya, 26, St. Petersburg, 194021, Russia
3 New Jersey Institute of Technology, University Heights, Newark, NJ 07102-1982, USA

Received 2019 January 16; revised 2019 July 28; accepted 2019 July 31; published 2019 September 18

Abstract

Particle acceleration in solar flares remains an outstanding problem in solar physics. It is currently unclear which of the acceleration mechanisms dominates and how exactly the excessive magnetic energy is transferred to nonthermal and other forms of energy. We emphasize that the ultimate acceleration mechanism must be capable of efficiently working in the most extreme conditions, such as the shortest detected timescales and the highest acceleration efficiencies. Here we focus on a detailed multiwavelength analysis of the initial phase of the SOL2011-08-04 flare, which demonstrated prominent short subpeaks of nonthermal emission during filament eruption associated with the flare. We demonstrate that the three-dimensional configuration of the flare, combined with timing and spectral behavior of the rapidly varying component, put very stringent constraints on the acceleration regime. Specifically, the rapid subpeaks are generated by short injections of nonthermal electrons with a reasonably hard, single power-law spectrum and a relatively narrow spread of pitch-angles along the mean magnetic field. The acceleration site is a compact volume located near the top of the extended coronal loop(s). The electrons are promptly accelerated up to several hundreds of keV, with the characteristic acceleration time shorter than 50 ns. We show that these properties are difficult to reconcile with widely adopted stochastic acceleration models, while the data inescapably require acceleration by a super-Dreicer electric field, whether regular or random.

Key words: polarization – X-rays: bursts – Sun: flares – Sun: radio radiation – Sun: X-rays

1. Introduction

Solar flares are, perhaps, the most powerful accelerators of charged particles in the solar system. However, in spite of extensive observational, theoretical, and modeling efforts over dozens of years, we are still far away from a detailed understanding of acceleration mechanisms and a clear scenario of how exactly the excessive energy stored in nonpotential magnetic field is converted during flares to other forms of energy, including nonthermal energy. In particular, the relationship between various timescales, ranging from very short, subsecond, to very long, multi-hour, is unclear. We do not know yet if subsecond episodes of particle acceleration are produced by the same or different acceleration mechanisms as compared with a more sustained acceleration that lasts from minutes to hours, if they occur in the same or different volumes, or if acceleration primarily occurs during these short episodes, while a more gradual component is a cumulative effect of many such episodes.

Acceleration episodes manifest themselves as distinct short subpeaks of hard X-ray (HXR) emission, which were proposed to represent a signature of direct precipitation of nonthermal electrons into the solar atmosphere dense layers. Those electrons were believed to be accelerated in discrete reconnection episodes in coronal structures of magnetic field (Kane et al. 1983). It was suggested that the duration of an elementary burst was controlled by the size of interacting current filaments (Sturrock et al. 1984; Larosa & Moore 1993), or by typical time of reconnection processes (Litvinenko 1996). Therefore, the flare configuration and time-of-flight relationships provide a basis for considering the acceleration process within the framework of either a “small-scale” model, which assumes that the electrons are accelerated promptly high in the corona and then precipitate down with constant velocities, or a “large-scale” model, which assumes that the electron acceleration is distributed over a large volume such as a significant portion of a flaring loop (Aschwanden 1996).

Whether within the small- or large-scale model, the mechanisms of particle acceleration in solar flares are still under debate and development. The list of proposed acceleration mechanisms is extensive: acceleration by DC electric fields in the coronal loops or in current sheets due to reconnection (Benka & Holman 1994; Zharkova & Gordovskyy 2004; Vlahos et al. 2016; Vlahos & Isliker 2019), betatron acceleration in collapsing magnetic loops (Somov & Kosugi 1997; Grady et al. 2012), acceleration in kink-unstable twisted magnetic loops (Gordovskyy et al. 2014), acceleration by Alfvén waves in loops (Fletcher & Hudson 2008), by shock waves generated by plasma outflows from the current sheet (Somov & Kosugi 1997; Mann et al. 2006; Nishizuka & Shibata 2013), resonant stochastic acceleration in small-scale fields of plasma turbulence (Miller et al. 1996; Petrovian & Liu 2004), acceleration by helical turbulence in the twisted magnetic field (Fleishman & Toptygin 2013), and nonresonant acceleration by strong large-scale turbulence (Bykov & Fleishman 2009).

HXR data provide the primary diagnostics of electron acceleration in flares, but it has severe limitations and biases. With a typical HXR spectrum falling with energy as a power law with reasonably large indices, \( \gamma = 3–8 \), the numbers of detected photons falls off quickly with energy such as it is impossible to either image the HXR sources or isolate short temporal HXR subpeaks from the noise above \( \sim 100 \text{ keV} \) in a typical flare. On top of that, the HXR emission intensity is weighted with the number density of the ambient thermal plasma; thus, the HXR images are typically dominated by chromospheric footpoints, where a so-called thick-target HXR emission is produced (e.g., Fletcher et al. 2011). In rare cases, the coronal portion of a flaring loop can be sufficiently dense...
of the order of $10^{11}$ cm$^{-3}$ or above) to render the loop collisionally thick for the accelerated electron. In such cases, coronal thick-target sources can be dominant (Guo et al. 2012), while the precipitation to the footpoints suppressed (see, however, Dennis et al. 2018).

A significant source of data that nicely complements the HXR diagnostics of the dynamics of electron acceleration comes from microwave observations, whose sensitivity to emission of nonthermal electrons in coronal magnetic structures is considerably higher (Altyntsev et al. 2012) compared with HXRs. Combination of spectral and imaging information in both HXR and microwave domains has already permitted us to pinpoint the flare energy release/electron acceleration regions in a few case studies (Meshalkina et al. 2004; Fleishman et al. 2011, 2013, 2016a).

It is important to realize that unlike HXR emission, which is produced by a single well-understood emission mechanism, bremsstrahlung, the radio emission can be produced by a rich variety of incoherent or coherent processes. This is especially true for short time structures, which often have a rather narrow instantaneous spectral bandwidth (Benz 1986; Zhelezniakov 1969; Altyntsev et al. 2007). Even a relatively tiny population of nonthermal electrons can produce such bursts by a coherent emission mechanism. On the contrary, broadband microwave background bursts, even having a rather short, subsecond duration, are believed to be generated by an incoherent gyrosynchrotron emission mechanism with, perhaps, a contribution from the free–free process (e.g., Altyntsev et al. 2008; Glesener & Fleishman 2018). Such gyrosynchrotron bursts are known to be extremely helpful in probing the magnetic field and nonthermal electron distribution (Gary et al. 2013, 2018).

The microwave continuum bursts last typically from several seconds to minutes (see, for example, Nita et al. 2004; Altyntsev et al. 2008; Fleishman et al. 2008; Lysenko et al. 2018), while those with a subsecond duration are detected more rarely (Kaufmann et al. 1980; Altyntsev et al. 2000; Meshalkina et al. 2004; Fleishman et al. 2016b; Glesener & Fleishman 2018), likely because the latter requires some special conditions to be met: (i) short and well separated episodes of electron acceleration; (ii) a high acceleration rate of electrons up to relativistic energies; and (iii) inefficient trapping of these electrons in the flaring coronal loops. However, when such subsecond subbursts are detected, their study can substantially narrow the list of possible acceleration processes given that only a subset of those processes will turn out to be capable of supporting that extreme acceleration efficiency at such short timescales.

It is intuitively clear that the acceleration processes can be more conclusively studied in flares with a relatively simple configuration of flare sources, in which no or only a weak trapping of accelerated electrons occurs and, thus, emission from the acceleration site directly dominates (see, e.g., Fleishman et al. 2011, 2016a).

In this work we study the primary energy release in the initial phase of the 2011 August 4 flare. The 2011 August 4 flare of GOES class M9.3 occurred in the central part of solar disk N17W37 (NOAA 11261) and reached its maximum at 03:56:30 UT. During a filament eruption prior to the flare impulsive phase, a unique sequence of broadband pulses was observed. We concentrate on analysis of a few episodes of short subsecond subbursts, both narrowband ones recorded in the radio domain only, and broadband subbursts recorded in both radio and X-ray domains, as compared with a more gradual underlying burst. We are specifically interested in characterizing spatial relationships between the sources of the short subsecond subbursts and source(s) of a more gradual emission and quantifying the sources in terms of their physical parameters (sizes, magnetic fields, number densities, etc.) with the goal of narrowing down the list of possible acceleration mechanisms.

2. Observations

As has been explained in the Introduction, we need to characterize a flare with as high spatial and temporal resolution as possible. This requirement motivates our selection of two imaging radio instruments working at three different microwave frequencies, and three different X-ray instruments, which collectively provide high spatial, spectral, and temporal resolution of the X-ray emission. This section provides an outline of the instruments and the data used in our study.

2.1. Instrumentation

2.1.1. Microwave Domain

The Siberian Solar Radio Telescope (SSRT) records one-dimensional (1D) radio images (scans) at 5.7 GHz with 14 ns cadence using east–west (EW) and north–south (NS) antenna arms (Altyntsev et al. 2003; Meshalkina et al. 2012). During the observations, the antenna beamwidth at the level of full width at half maximum (FWHM) was 18" and 20" in the EW and NS directions, respectively. We employed fast SSRT light curves to identify short subpeaks with the duration of less than, or about, a second. Fast 1D scans were used to study locations of the subpeak sources. SSRT also produces two-dimensional (2D) images of a solar disk every 2–3 minutes (Grechnev et al. 2003; Kochanov et al. 2013). 2D images were used to study the morphology and location of the background microwave burst source.

The Nobeyama Radio Heliograph (NoRH; Nakajima et al. 1994) produces full-Sun 2D images at 17 GHz (intensity and polarization) and 34 GHz (intensity only) with the 0.1 s cadence. The NoRH spatial resolution was 13" at 17 GHz and 8" at 34 GHz at the time of the flare under study. The imaging was employed to study locations and morphology of the flare at high frequencies. To study the fast source dynamics we used imaging with the highest possible 0.1 s cadence.

The Nobeyama Radio Polarimeters measured the total power (TP) radio emission at six microwave frequencies from 1 to 35 GHz with the cadence of 0.1 s (NoRP; Torii et al. 1979). We used the NoRP data to study the evolving microwave spectrum. However, given a rather weak signal at 35 GHz, we also employed the cross-correlation curves of the longest NoRH baselines to recover evolving radio flux of the burst at 34 GHz.

2.1.2. X-Ray Domain

The Reuven Ramaty High-Energy Solar Spectroscopic Imager (RHESSI; Lin et al. 2002) records individual photons with high spectral resolution between 3 keV and 17 MeV with nine front and nine rear detectors. RHESSI employs rotational synthesis imaging technique possible due to spacecraft rotation with 4 s; thus, higher time resolution light curves are not easily available. We employed the RHESSI data to produce X-ray
images and spectra of the sources of the smooth emission component, while we used two other instruments to study the fine temporal structure of X-ray emission.

The Fermi Gamma-Ray Burst Monitor (GBM, Meegan et al. 2009) is one of the instruments on board the Fermi Space Telescope (Atwood et al. 2009), which provides the light curves in the spectral range from ~8 keV to ~40 MeV with temporal resolution of 256/64 ms, while the GBM spectra were available with the cadence of 1.024 s. The detector area is 128 cm².

The Spectrometer KONUS on board of the Wind spacecraft (Konus-Wind; Aptekar et al. 1995) works in either waiting or triggered mode. The detector area is ~100 cm². In the triggered mode, employed here, the light curves are recorded in three energy bands (G1 18–75 keV, G2 75–308 keV, and G3 308–1050 keV in the event under study) with variable time resolution from 2 to 256 ms. Multichannel spectra are taken over uneven time intervals, whose duration is determined adaptively depending on the count rate and varies between 64 ms and ~8 s. We employed the time domain Konus-Wind data to study variations of the HXR spectral hardness with a subsecond time resolution.

2.1.3. Context Data

The Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board the Solar Dynamics Observatory (SDO) is a narrowband UV imager that records full-disk solar UV/EUV emission in 10 narrow passbands with 1/5° angular resolution and 12 s cadence. We employed the AIA imaging data in a few “coronal” passbands sensitive to hot plasma to investigate the flare morphology.

The Helioseismic and Magnetic Imager (HMI; Scherrer et al. 2012) on board the SDO provides full-disk solar magnetograms, dopplergrams, and white-light images with a subarcsecond spatial resolution and 45 s to 12 minute time cadence depending on the data product. In this study, we employed full-disk vector magnetograms to initiate 3D modeling of the flare.

2.1.4. Analysis and Modeling Tools

In most cases, standard SSW analysis tools were used. In particular, the RHESSI data were analyzed with the OSPEX and the imaging software developed by the RHESSI team (Lin et al. 2002), which permits obtaining spectra, full-disk light curves, and images at various energy bands, and performs spectral fits.

GX Simulator (Nita et al. 2015, 2018) is an interactive tool (an IDL-based widget freely distributed via SSW) developed for 3D modeling of active regions and solar flares. It supplants the user with the possibility of automated production of a 3D magnetoplasma data cube built for a user-defined field of view and spatial resolution. The 3D magnetic model is created by nonlinear force-free field (NLFFF) reconstruction (Fleishman et al. 2017) initiated with the corresponding photospheric vector magnetogram automatically downloaded from the HMI/SDO site. We employed the GX Simulator for 3D modeling of the flaring loops and computation of the associated electromagnetic emission.

2.2. X-Ray and Microwave Light Curves

Figure 1 displays a representative subset of the X-ray and microwave light curves. A few series of short subpeaks with duration about a second are seen at the initial stage of the flare. To highlight weak emission enhancements before the main flare phase, we use the log scale for the radio light curves. The time ranges of the fast variations are marked by the vertical lines in Figure 1: group I (03:44:15–03:44:22 UT), group II (03:45:00–03:45:54 UT), and group III (03:49:00–03:49:08 UT). The time profiles of the smoothed (background) microwave emission are overall similar to each other in a rather broad range of frequencies, 1–35 GHz, which favors a single incoherent mechanism of the background emission. The soft X-ray emission raised slowly at the initial stage of the flare.

Groups I and II occurred a few minutes before the flare impulsive phase. During the first group there were subpeaks with a “one-to-one match” correspondence between pulses at 5.7 and 17 GHz, and HXR emission pulses. The NoRP data with the time resolution of 0.1 s are not available and this group was too weak for quantitative analysis. More detailed and reliable data are available for the second group of the subpeaks. The subpeaks of the second group were reasonably strong as they occurred during the microwave burst with flux density reaching hundred of sfu at 3.75–9.4 GHz.

The third group occurred later, at the beginning of the flare impulsive phase, while at 5.7 GHz only. Several oscillations of emission flux with an approximately 0.5 s period occurred during 8 s. Unlike previous intervals with the subpeaks on NoRP and HXR light curves, no counterpart to the oscillations at 5.7 GHz was observed at either NoRP or HXR light curves. We conclude that in this case, the subsecond pulses are narrowband and, thus, are likely generated by a coherent mechanism.

Let us study the second group in more detail (Figures 2 and 3). There is a “one-to-one” correspondence between individual peaks in the HXR and microwave emission. The subpeak durations (the time intervals between signal minima) are within the range of 0.7–1.8 s. Figure 2 presents the GBM-Fermi light curves recorded with 64 ms bins. The calculated errors are in range from 16 to 36 counts/s in the GBM channels. The reliability of the short pulses in hard X-rays is confirmed by the comparison of time profiles recorded by the GBM and Konus-Wind. The Konus-Wind data in the triggered mode are available after 03:45:27.5 UT. The Konus-Wind profiles (Figures 2(c) and (d), dotted curves) are smoothed with a window width of 256 s, and the amplitudes are normalized to the amplitudes of the GBM profiles.

The hard X-ray subpeaks stand out cleanly at two energy channels: 26.7–50.3 keV and 50.3–102.2 keV, where their amplitudes are comparable with that of the more gradual background component. To aid the eye to see the correlation between various light curves, the vertical lines mark times of the most prominent subpeaks with duration about 1 s in the GBM 26.7–50.3 profile (Figure 2(c)). In this channel the GBM rates are sufficiently large (>1000 counts/s) to separate the subpeaks. At lower energy channels the subpeaks are less pronounced. At 102.2–293.5 keV the count rate is lower and the peak correspondence is apparent for large peaks only. Reliability of the subpeaks is confirmed by the Konus-Wind records. There is a clear correspondence between the profiles in Figure 2(c). Correlation is lower in Figure 2(d) in energy channels G2 (75–308 keV), while channel G3 is not

---

4 Data for all flares registered by Konus-Wind in the triggered mode are available online via http://www.ioffe.ru/LEA/kwson/.
shown because there is no significant signal above the level of statistical fluctuations.

The microwave light curves in Figure 3 were obtained with the NoRP at 1.0, 2.0, 3.75, and 9.4 GHz, and by the SSRT at 5.7 GHz, while the NoRP data at 17 and 35 GHz were too noisy. For that reason, we employed the NoRH data at 17 and 34 GHz. The dotted curves in panels (f) and (g) are obtained by integrating the sequences of NoRH images over the field of view. This technique worked well with the original 0.1 s cadence at 17 GHz, while it did not work at 34 GHz due to significantly lower signal-to-noise ratio. Thus, in panel (g), the dotted curve shows the radio flux obtained with 1 s cadence and then smoothed with 3 s cadence, which is insufficient to resolve individual subpeaks. To recover the subpeaks at 34 GHz, we employed the NoRH correlation plots involving only the longest baselines, which are only sensitive to the most compact sources of emission. The validity of this approach is confirmed by 17 GHz data, where the profiles of the normalized correlation plots (solid) and the fluxes (dotted) closely match each other; thus, the correlation plot can be straightforwardly renormalized to represent the burst flux in sfu. The corresponding solid curve in panel (g) also matches the dashed one on average, while recovering the fine temporal structure at 34 GHz. Thus, the noise levels do not exceed 5% at all frequencies except 34 GHz, where it is two times larger. As in the HXR case, the profiles become smoother at the lower frequencies. Note, however, prominent short, narrowband subpeaks at 1 GHz numbered 7 and 12, which are likely produced by a coherent mechanism. The observed microwave spectrum is typical for gyrosynchrotron emission with a spectral peak within the 5.7–9.4 GHz range (Nita et al. 2004). Thus, the microwaves and X-ray light curves at the frequencies 5.7–17 GHz and energies 26.7–102.2 keV are similar to each other at all timescales, including the subsecond structure.

Although the light curves at various frequencies/energies are highly correlated, they show measurable delays between each other. To quantify the time lags, all light curves, during the time interval of 03:45:15–03:45:55 UT, were interpolated down to 14 ms cadence to match the best available time resolution provided by SSRT data. From the resulting time profiles, we subtracted the running mean with a 2.1 s smoothing window and computed the lag correlation between the light curves (see Table 1). The correlation coefficient and
the delay values depend on the width of the smoothing window only slightly. Within smoothing windows of 1.3–2.8 s, the calculated delays are within the error limits in Table 1. The last column contains estimates of the "weighted" energy of emitting electrons. The obtained correlation coefficients are high except for the 4.3–11.6 keV channel. In all cases, the calculated delays were significantly shorter than the subpeak duration. In the HXR domain, the subpeaks at low energies occur a few dozens of milliseconds later than those at the high energies. The microwave light curve at 5.7 GHz is delayed by roughly 70 ms, while those at 17 and 34 GHz by roughly 120 ms relative to the 102.2–293.5 keV channel.

The subpeak durations in the photon energy range of 26.7–293.5 keV is within 0.7–1.8 s, while the rise and decay times are comparable to each other. This property alone tells us that the electron transport in this event necessarily includes precipitation to the chromospheric footpoints. Indeed, such a rapid decay of the HXR emission requires accordingly rapid collisional losses of the nonthermal electrons with energy of several hundred keV, which can only happen in a dense chromospheric footpoint plasma, rather than in the coronal portion of the flaring loops. Specifically, to ensure the collisional loss time of less than 0.5 s, the plasma density should exceed $2 \times 10^{12} \text{ cm}^{-3}$ (Trubnikov 1965), which is unavailable in the coronal portion of the flaring loops.

2.3. Configuration of the Sources

Spatial structure of the sources, their relationships, and sizes are of primary importance to quantify electron acceleration in flares. Overall contextual information about the flare morphology and, to some extent, its dynamics, can be obtained from EUV data. Zuccarello et al. (2014) investigated evolution of this active region, NOAA 11261, during several days prior to the flare. There were three leading spots of the south polarity and a tail plage with the northern magnetic field. Two days before the flare under study, a filament appeared in 193 and 304 Å passbands along the neutral line. It destabilized on August 3, after M6.0 flare at 13:17 UT, when the filament’s western end began propagating toward the south. On August 4, the process of filament elongation and rise accelerated and the

Figure 2. Interval II. Intensity of HXR emission in channels GBM (black curves) and Konus-Wind 18–75 and 75–308 keV (red curves). Konus-Wind data in fast mode are available after 03:45:27.5 UT. Rate in counts/s. The Konus-Wind values are normalized to the GBM ones by multiplying by factors 0.8 (c) and 2.2 (d). Vertical lines mark the prominent subpeaks.
onset of the filament eruption occurred at 03:36 UT and it fully erupted after 03:48 UT.

A set of bright EUV loops showed up in the vicinity of the filament southern tip after 03:36:20 UT. The first microwave enhancement likely associated with the filament rising. Group I of the subpeaks, appeared after 03:44:15 UT. Figure 4 displays the microwave sources in the context of the photospheric magnetogram and coronal loops seen in EUV. Figure 4(a) shows the 50% contours of the microwave sources at three frequencies during the subpeaks of the Group II interval. The SSRT 2D-image, shown in red, is obtained at the end of the interval. It is apparent that the 5.7 GHz source is elongated along the neutral line of the contrast-enhanced magnetogram. The length of the emission region is about 55″ (hereafter, the low-frequency, LF-source). This apparent length is three times larger than the SSRT beam, which was about 20″; thus, the true LF-source length can be estimated as roughly 40″. The apparent width of the source is comparable with the FWHM of the SSRT beam; thus, the true width does not exceed several arcseconds. Therefore, the LF-source can be tentatively identified with an extended loop.

Unlike the elongated emission source at 5.7 GHz, the sources at 17 and 34 GHz are not spatially resolved: they have an almost circular shape with the sizes comparable with the NoRH beam sizes. Given that the source size was about 10″ at 34 GHz, where the beamwidth was about 8″, the true source size can be estimated as ≈5″. Thus, two spatially distinct sources of the background burst can be identified in the microwaves: an elongated LF-source, and a compact high-frequency HF-source. As follows from Figure 4(b) the LF-source covers the southern part of the rising filament. The HF-source projects on the 131 Å image area, where two small bright ribbons can be distinguished.
In Figure 5, the HXR sources are shown in two energy bands. The underlying image shows the map of He II-line-dominated 304 Å emission at 03:45:35 UT, which is the AIA channel most sensitive to the low-temperature plasma of the rising filament. The brightness center of the 25–50 keV source is located near the HF-source, but there is an elongated area of the emission along the LF-source. Its length is about 35″ in the north–south direction. At 6–12 keV, a presumably thermal, compact source (of about 10″) projects on the location of the HF-source.

In the second panel the contours of circularly polarized emission at 5.7 GHz are shown. The region of the polarized emission is extended along the LF-source, whose intensity (Stokes I) is shown as the color image background. The polarization is left-handed everywhere with the degree of polarization below 10%. The polarization of the 17 GHz source is also left-handed with the degree of polarization at about 20%.

Taken at face value, this combination of images is consistent with a single flaring loop elongated in the north–south direction. The single-loop interpretation, however, suggests a rather unusual placement of the X-ray sources. Indeed, in such a case, the low-energy thermal source would be associated with a footpoint of the loop, while the high-energy nonthermal source would be elongated along the loop, which is exactly opposite to what is expected and typically observed. Therefore, we propose that the thermal X-ray source is associated with compact unresolved flux tubes, while the HXR emission comes primarily from footpoints of other loops elongated in the north–south direction. We further propose that the LF-source is associated with these elongated loops, while the 17 GHz source is associated with the other (northern compact) loops, which produces thermal X-ray emission.

It is further important to quantify the spatial configuration of the sources that generate the short subpeaks of emission and compare it with the configuration of the source of the
background bursts. Unfortunately, the X-ray imaging available from RHESSI cannot be performed at the required short timescales. However, microwave imaging can be made with sufficient cadence to study the subpeak sources. The SSRT scans (see Section 2.1.1) provide the source spatial structure with the cadence of 14 ms. The NS scans are available over the whole length of Group II, but the EW scans are recorded during the interval with subpeaks \# 1–6. Figure 5(b) shows the scans during a subpeak marked \# 2 in Figure 3, when the scans were available from both SSRT antenna arms. The subpeak component was obtained as the difference of the scans at the very peak and at the previous valley. The scans along the flare loops recorded by the NS arm show a more elongated source than the EW scans. The scan along the flare loops recorded by the NS arm shows a more elongated source than the EW scan. The size of the subpeak source is comparable with the size of the background LF-source. The transverse size slightly exceeds the EW beam, so the actual width of the subpeak source can be estimated as 10″. Note that there is a brightness depression approximately at the center of the NS scan. The depression length is about 20″, which is the FWHM of the NS beam. In order for such depression to be observed, the real length of the depression must be \( > 25″ \). Thus, the sources of subpeak emission are adjacent to the loop footpoints. 1D brightness distributions are close for all subpeaks, and the position of the depression fluctuated at different subpeaks within 2″–8″ along the NS scan, while within less than 4″ along the EW scan. Brightness on the sides of the depression varied; however, they changed synchronously with accuracy better than 10 ms and a high correlation between the spatially resolved light curves from the northern and southern regions with the correlation coefficient of 0.88. The double structure of the synchronous LF-source brightening is likely critical observational evidence of particle acceleration in/above the depression area seen in the NS scans.

The subpeaks at 17 GHz were produced at the HF-source. So, the position and size of the sources of broadband subpeaks are close to those of the background sources at all frequencies. However, despite the similarity of the time profiles, the sizes and locations of the sources of subpeaks at 5.7 and 17 GHz were significantly different from each other. These relationships imply a common acceleration region of the nonthermal electrons, but a rather complicated transport of the electrons in involved flaring magnetic flux tubes.

The third group of subpeaks is rather different. The low-intensity broadband subpeaks were produced from a compact source located in the LF-source (Figure 5(b)). Within the uncertainty introduced by the SSRT beam size, the estimates yield the size of the source of a few arcseconds. This group of subpeaks does not have any counterpart at other frequencies or HXR energy channels.

2.4. Spectral Properties in X-Ray and Microwave Emission

Now, after the temporal and spatial properties of the flaring sources have been established, we turn to the corresponding spectral properties emphasizing distinct spectral properties of the subpeaks. Variation of X-ray hardness is quantified using the Konus-Wind data (Figure 6). The fourth panel of this figure shows the ratio of count rate time profiles in G1 and G2 channels. The ratio decreases during subpeaks, i.e., the subpeak spectrum is harder compared to the background burst spectrum indicating the soft–hard–soft (SHS) pattern similar to other studies of HXR subsecond variability (e.g., Fleishman et al. 2016b; Glesener & Fleishman 2018).

In order to determine properties of the electrons accelerated during the HXR subpeaks, let us compare the spectra at a subpeak maximum and a valley. Figures 7(a) and (c) show the spectra obtained for subpeaks \# 7 and \# 9 near the maximum of X-ray signal and for the deep valley between subpeaks \# 9 and \# 10. The spectra were computed from the GBM data using the OSPEX package for the most appropriate 1 s intervals. Subpeak \# 9 occurred directly in front of the valley, while subpeak \# 7 is the brightest one. The intervals with the valley and the subpeak \# 7, 9 are shown by the gray vertical strips in Figure 6. For each time interval we subtracted the time-dependent background from the GBM signals.

The spectra show typical shapes consistent with a thermal core and nonthermal tail, which can be fitted with a thermal component at low energies and with a broken power-law component at high energy. The temperatures at the valley and at the subpeaks are 30 MK and 37 MK, respectively. The power-law break energies are 44 keV for the valley and 66–73 keV for the peaks, above which the spectra become softer with indexes \( \approx 4.2 \). The power-law indexes under the break energies are 2.3–2.4 and are slightly higher at the time of the subpeaks. Puzzling is the fast change of the plasma temperature suggested by the thermal part of the fit. Indeed, the timescales of the plasma heating and cooling are typically much longer than the subsecond timescales of the electron acceleration, so that fast jumps of the plasma temperature look suspicious. We challenge this straightforward interpretation of the fit results by computing the difference between the spectra at the peaks and at the valley (Figures 7(b) and (d)). It is seen that their difference in the range between 8 and 120 keV is a power-law function of the photon energy that can be approximated with functions \( (2.7 \pm 0.5) \times 10^{3} E^{-2.38 \pm 0.05} \) (subpeak \# 7) or \( (1.4 \pm 0.6) \times 10^{3} E^{-2.36 \pm 0.11} \) (subpeak \# 9), where \( E \) is expressed in keV. A similar picture is seen for other peaks, although weaker peaks show larger associated uncertainties.

Thus, our interpretation of the spectrum evolution is as follows: there is a slowly varying background emission, which consists of a thermal component (\( T \approx 30 \) MK) and a broken power-law component, on which a new population of freshly accelerated electrons with a single power-law spectrum is superimposed during the peak.

Complementary, evolution of the microwave-emitting electrons can be quantified by time variation of the ratio of radio fluxes in the optically thin part of spectra. The last panel of Figure 3 shows the flux ratio at 34 and 17 GHz. It goes up on average and, thus, the hardness of radio-emitting electrons is slowly increasing on average during interval II with subpeaks. There is no clear spectral variation pattern associated with subpeaks, which is, perhaps, hidden by a high level of ratio fluctuation. To isolate the contribution to the microwave radiation of electrons injected during the subpeaks, let us consider the spectrum of the largest subpeak in microwaves (# 8) in comparison with the valley emission in front of it (Figure 8). The inverted bell shape of the spectra is typical for the gyrosynchrotron emission. Both spectra are flat in the 3.75–9.4 GHz range, which evidences the contribution to the emission of more than one source or, in a general case, of a spatial nonuniformity of the source (Lee & Gary 1994; Altyntsev et al. 2016; Fleishman et al. 2016b). The spectrum
shapes are similar before and at the subpeak, but the difference is weaker at the optically thick part at low frequencies. At the 8th subpeak, for example, the flux intensities are rising up by 30%–50% in the frequency range 3.75–9.4 GHz. We conclude that the overall spectral trends revealed from the microwave and HXR data are consistent between each other and consistent with the idea of new injections of the nonthermal electrons during the subpeaks.

2.5. Summary of Observations and Implications

The main results for the broadband subpeaks considered here can be summarized as follows:

1. Configurations of the broadband subpeak and background burst sources are similar to each other. This configuration consists of two structures. The first structure (LF-source) is seen at 5.7 GHz emission and corresponds to loops elongated from the north to the south for 40°. The second one is a compact source, which is only several arcseconds in size located at the northern end of the LF-source. This HF-source is observed in microwaves at 17 and 34 GHz and in the X-rays. This source is, most likely, associated with a compact flux tube. The high-energy, 26.7–50.3 keV, X-ray source displays an elongated structure with a length of 35°, superimposed on the LF-source in the picture plane.

2. Durations of the subpeaks are within the range of 0.7–1.8 s. The short duration and symmetry of the temporal profiles of the subpeaks imply an important role of the scatter-free propagation of the nonthermal electrons in the loops.

3. The HXR pulses with photon energy above 100 keV lead the lower energy X-ray light curves. Delays in the HXR emission grow as the energy decreases and reach 70 ms at low energies. The microwave emission is delayed relative to HXR. The delay at 5.7 GHz is ∼70 ms, while at 17 and 34 GHz is ∼120 ms relative to 102.2–293.5 keV X-rays.

4. There are two sources of subpeak emission at 5.7 GHz, which are adjacent to the footpoints of the loop. Their relative brightness varied synchronously, which implies that the electrons are injected from an acceleration region located at/near the looptop toward both footpoints of the loop associated with the LF-source.

5. X-ray spectra show SHS behavior during subpeaks. The difference spectrum indicates that such a behavior in the

---

**Figure 6.** Time profiles of count rate time profiles in the Konus-Wind energy channels G1 (18–75 keV), G2 (75–308 keV), G3 (308–1050 keV), and the ratio G1/G2. Temporal resolution is 512 ms. The gray vertical strips show the intervals of the Fermi-GBM spectrum calculation.
3. Discussion

The observed remarkable similarity between the radio and X-ray light curves at all timescales from less than a second to several minutes along with revealed spatial relationships between sources of short peaks and a more gradual background, imply a common origin of the populations of emitting nonthermal electrons producing both the background burst and the subpeaks. It is natural to interpret the subpeaks as signatures of fast acceleration of electrons, a significant fraction of which is then rapidly lost from the source. To nail down the acceleration mechanism responsible for these short acceleration episodes and their role in forming the nonthermal component of the solar flare, we have to quantify the acceleration rate, the spectrum, and the number of accelerated electrons, as well as the electron transport in the flaring volume.

3.1. Flare Configuration

To investigate the likely topology of the coronal sources (loops) involved in the flare, we employ 3D modeling with the GX Simulator (Nita et al. 2015) based on NLFFF reconstruction using the weighted optimization code described and validated by Fleishman et al. (2017). This NLFFF reconstruction is now a part of the automated model creation pipeline included in the SSW distribution of the GX Simulator (Nita et al. 2018). The NLFFF reconstruction is initiated with the SDO/HMI vector magnetogram taken before the flare onset at 03:34:26 UT. The modeling approach is described in detail in a number of recent publications, (see, e.g., Fleishman et al. 2018; Kuroda et al. 2018, and references therein). Specifically, we are looking for magnetic structures consistent with imaging data at the microwave and X-ray domains, which form the corresponding flaring flux tubes, and then populate them with the thermal plasma and nonthermal electrons such as the synthetic microwave and X-ray emissions, computed from the model, match the observations (both images and spectra).

For our case, the relevant extrapolated magnetic lines forming distinct flux tubes are presented in Figure 5(c). At least two loops are unavoidably needed to reproduce the source morphology (see Section 2.3). The two selected loops, whose main parameters are summarized in Table 2, permit a reasonable agreement of the calculated microwave spectrum with the observed background microwave spectrum (Figure 8). Within the model (Figure 5(c)), small Loop I is associated with the HF-source, while Loop II is associated with the extended LP-source.

As has already been noted, the nonthermal electron transport in this event is dominated by a scatter-free propagation. This implies that a “trap plus precipitation” (TPP) model (Melrose & Brown 1976) could be a good approximation for our case. The main feature of this model is a critical pitch-angle of the

![Figure 7](image-url). (a, c) Spectra of HXR emission recorded by the GBM during the 9th and 7th subpeaks (black) and during the valley between subpeaks #9 and #10 (gray). The dotted lines show the background levels. (b, d) The differences of these spectra (crosses) and a linear function approximation (dashed). The corresponding time intervals are blackened in Figure 7.
nonthermal electron population, which demarcates fractions of precipitating and trapped electrons. Figure 8 shows the relative delays between different HXR channels as a function of the “weighted” energy of the nonthermal electrons that make dominant contribution to a given HXR channel. These weighted energies (see the fourth column of Table 1) were determined based on the algorithm developed by Aschwanden & Schwartz (1996) for a power-law distribution of nonthermal electrons, which we employed for the case of the photon spectral index $\approx 2.4$ (see Section 2.4 for detail). The measured delays are remarkably consistent with the energy-dependent TOF delays of electrons, which are simultaneously injected into a flaring loop, after propagation over a distance of $L_{\text{TOF}} \approx 20 \text{ Mm}$ (shown in Figure 8 by the solid curve) toward the footpoints; this behavior is similar to a few cases described by Aschwanden et al. (1996). We note that this “toy TOF model” in its simplest form ignores a number of potentially important physical effects, such as field helical twist of the magnetic field, pitch-angle distribution, evolution of the injected energy spectrum, and potential deviation of the electron transport from the free-streaming mode, any of which can reduce the actual TOF length estimate.

Indeed, the half-length of large loop II is about 11 Mm (see Table 2), which is in apparent contradiction with the TOF distance (20 Mm) revealed by the delay analysis (Figure 9). Brown et al. (1998) demonstrated that a certain type of spectral evolution of the nonthermal electrons precipitating at a footpoint can emulate the same energy-dependent time delays as expected from the TOF propagation even without any propagation (i.e., when the injection occurs just above the footpoint). Such an extreme is clearly inconsistent with our imaging data. In particular, the fact that the microwave subpeaks at two legs of the large loop are synchronous, mentioned above in Section 2.3, unambiguously places the acceleration/injection site at a coronal location at or above the looptop. Having said that, we note that some spectral evolution of the electrons injected at the looptop along with the pitch-angle distribution can still affect the exact delay values, while the field inclination is taken into account within our 3D model. We checked that an SHS evolution of the injected nonthermal electron spectrum, where the spectral index varies by a few percent, while the electrons are beamed along the magnetic field can reduce the TOF distance by a factor of two as needed. However, such a model does not contain any population of nonthermal electrons reflected back to the coronal portion of the flaring loop(s) needed to account for the microwave emission. From this, we conclude that an electron beam with a modest angular scatter, rather than an ideal field-aligned beam, is responsible for the observed deviation of the loop half-length from the estimated TOF distance.

Such an angular distribution is capable of reducing their “effective” speed along the magnetic field typically by a factor of 1.5–3. As we noted above, some angular spread is also required to supply a population of the upward-reflected electrons needed to interpret the microwave data. However, an isotropic angular distribution does not look likely given that there is a rather large pitch angle of the majority of streaming electrons and, thus, efficient trapping, which is not observed. Thus, the data favor an anisotropic beam-like distribution of the accelerated electrons with a modest opening angle of $30^\circ$–$40^\circ$.

The mirror ratio $m = 3$ in Loop II of our 3D model; thus, the electrons launched downward at the pitch-angle $\vartheta \lesssim 35^\circ$ will not be reflected at the footpoint and, thus, will not contribute to the trapping. The mean parallel velocity $v_{||}$ for the electrons launched at the looptop at $\vartheta = 35^\circ$ is $v_{||} \approx v \cos \vartheta / 2 \approx 0.4v$. Electrons with $\vartheta \gtrsim 35^\circ$ will be reflected and will contribute to the brightness peaks observed at 5.7 GHz from the LF-loop. The observed delay of 70 ms between 5.7 GHz peaks and 102.2–293.5 keV emission peaks, both produced by presumably 400 keV electrons, places the 5.7 GHz source at a distance $\sim 5 \text{ Mm}$ from the mirror points at the bases of loop II. Microwave emission at 17 and 34 GHz delayed by 120 ms requires an additional time for the electrons to be transported from Loop II to Loop I and, perhaps, additional time for trapping in Loop I.

Thus, the time delays are naturally consistent with the identified magnetic configuration of the flare and the TPP model in which the particles are injected at the looptop of Loop II and then propagate to produce the observed variety of the HXR and microwave components.

3.2. Accelerated Electron Population

In Section 2.4 we determined the HXR spectrum of subpeaks to be a single power-law with the indexes about 2.4. This spectrum is injected during a subpeak in addition to a preexisting population of nonthermal electrons responsible for a gradual (background) component of the burst. In the thick-target model (Hudson et al. 1978), the high-energy part of the photon spectrum is produced by the electron flux of $(0.8–3.2) \times 10^{37} E^{-3.4} \text{ electrons keV}^{-1} \text{s}^{-1}$. The total flux of nonthermal electrons above 20 keV, commonly used as a reference energy, can be estimated in this case as $\phi'(\geq 20 \text{ keV}) \approx (0.6–2.4) \times 10^{34} \text{s}^{-1}$ during the subpeaks.
is the mean electric field. The density of nonthermal electrons emitting the microwaves during a subpeak does not exceed \(2 \times 10^{32}\), which is only a few percent of the number of electrons accelerated per pulse. This agrees with the earlier obtained conclusions of relatively inefficient electron trapping in this event and further indicates a reasonably small range of pitch angles of the accelerated electrons.

### 3.3. Acceleration Mechanism

The spatially resolved microwave data place the acceleration region somewhere in the middle of the extended LF-source. Given that regardless of the specific acceleration mechanism, the only force capable of accelerating charged particles is the electric force, the net electric field (whether regular or stochastic) has to do the required work \(A = E L_{\text{acc}}\) on the electron to accelerate it up to half MeV, where \(A \sim 0.5\) MeV and \(E\) is the mean electric field along the acceleration path.

Let us estimate the upper bound of the acceleration length \(L_{\text{acc}}\) from the timing of the acceleration. Given that the timing of the HXR subpeaks is fully consistent with the timing of precipitation, the acceleration time \(\tau_{\text{acc}}\) up to high energies must necessarily be much shorter than \(\tau_{\text{TOP}} \sim 85\) ms, thus, necessarily \(\tau_{\text{acc}} < 50\) ms. The acceleration time \(\tau_{\text{acc}} < 50\) ms implies the acceleration region size \(L_{\text{acc}} \sim \langle \psi \rangle \tau_{\text{acc}} < 10\) Mm, where \(\langle \psi \rangle \approx 2 \times 10^{10} \text{ cm s}^{-1}\) is the mean velocity of the electron during the acceleration up to roughly half MeV. For the estimated above upper bound of \(L_{\text{acc}} \approx 10\) Mm, we find the required accelerating electric field \(E > A/L_{\text{acc}} \sim 0.1\) V m\(^{-1}\), which is at least one order of magnitude larger than the typical values of the Dreicer field (\(\sim 10^{-2}\) V m\(^{-1}\)).

Super-Dreicer electric fields are both expected (Priest & Forbes 2000) and implied by the data analysis (Qiu et al. 2009; Fleishman et al. 2016b). However, how exactly these fields drive acceleration of electrons remains very poorly understood. Most likely, a turbulent reconnection environment is formed somewhere at the flare cusp region (Vlahos & Isliker 2019), where multiple current sheets are formed randomly. The reconnection-driven decay of the magnetic field is associated with the electric field according to Faraday equation \(\dot{B} = -\mathbf{e} \nabla \times \mathbf{E}\), which, in its turn, accelerates electrons to high nonthermal energies. A well-known problem with a traditional acceleration in super-Dreicer electric field in a single current sheet is the difficulty of obtaining a power-law spectrum of the nonthermal electrons. In case of the turbulent reconnection with many current sheets involved, the statistics of accelerated electrons may simply follow the statistics of the electric field in the range of available current sheets; thus, if the electric field is distributed over a power law, the spectrum of the accelerated nonthermal electrons will also follow a power law (Vlahos & Isliker 2019). In addition, in agreement with

\[\text{Figure 9. Time delays in various HXR energy channels.}\]

Now we address the question of whether such injections are capable of naturally reproducing properties of the microwave subpeaks. To do so, we develop a simplified two-component model guided by imaging data and parameters revealed within 3D modeling. This simplified modeling employs the fast GS code developed by Fleishman & Kuznetsov (2010) to compute the microwave emission from two uniform sources with sizes consistent with the SSRT and NoRH maps. Figure 8 and Table 2 present the best simulated spectra of the background microwave emission and associated physical parameters of the sources. These modeling parameters are broadly consistent with the parameters of the flaring volume obtained with the 3D modeling. In particular, the magnetic fields of 250 and 500 G for the LF- and HF-sources are, respectively, in the ranges of the corresponding magnetic field in the 3D model.

This simplified modeling shows that the increase of emission by 30%–50%, as observed during subpeak \# 8, can be explained by roughly doubling the density of nonthermal electrons above 20 keV. The increase of the total number of electrons emitting the microwaves during a subpeak does not exceed \(2 \times 10^{32}\), which is only a few percent of the number of electrons accelerated per pulse. This agrees with the earlier

\[\text{Table 2: Source Parameters Derived by Fitting Background Microwave Spectra}\]

| Source          | 3D GS-Simulator | GScode |
|-----------------|-----------------|--------|
| Loop I          |                  |        |
| Loop II         |                  |        |
| Size [Mm]       |                  |        |
| Magnetic field (top) [G] | 15.3 × 3 × 3 | 10511 |
| Magnetic field (N-footpoint) [G] | 600 | 916 |
| Magnetic field (S-footpoint) [G] | -1554 | -390 |
| Plasma density, \(n\) [cm\(^{-3}\)] | 1.5 × 10\(^{10}\) | 4.3 × 10\(^{10}\) |
| Power index, \(\delta\) | 2.4 | 10\(^{10}\) |
| Density of nonthermal electrons (>20 keV) [cm\(^{-3}\)] | 8.4 × 10\(^{5}\) | 3 × 10\(^{6}\) |
| Number of nonthermal electrons | 1.2 × 10\(^{32}\) | 2.3 × 10\(^{12}\) |
observations, such a model can naturally produce a beamed distribution of the accelerated electrons following the preferred direction of the electric field in this collection of the turbulent current sheets, while conventional stochastic acceleration mechanisms tend to produce much more isotropic distributions due to efficient angular scattering of the particles by turbulence.

4. Conclusions

The study of the source morphology complemented with the analysis of timing and spectrum of the subsecond emission peaks, performed above, has revealed striking properties of the acceleration process. Indeed, we found that the electrons are accelerated promptly (the acceleration time is shorter than 50 ns) up to several hundreds of keV, which is difficult to reconcile with conventional stochastic acceleration models.

These electrons propagate freely along the flux tube, which implies no (or only weak) wave–particle interaction unlike many other cases (e.g., Fleishman et al. 2018), where turbulence was found to play a central role in particle acceleration and transport. On the other hand, the observations are broadly consistent with the predictions of models that invoke large, super-Dreicer, electric fields.

The work was supported by the Russian Science Foundation (project No. 18-12-00172). G.F. (Discussion) acknowledges support by NSF grant AGS-1817277 and NASA grants 80NSSC18K0667 and 80NSSC18K1128 to New Jersey Institute of Technology. A.L. (Konus/\textit{Wind} data analysis) acknowledges support from RSF grant 17-12-01378. N.M. (NoRP data analysis) acknowledges support from the Program of basic research of the RAS Presidium No. 28. We are grateful to the teams of the Siberian Solar Radio Telescope, Nobeyama Radio Observatory, \textit{SDO}, \textit{RHESSI}, \textit{FERMI}, and Konus/\textit{Wind} who have provided open access to their data. The experimental data were obtained using the Unique Research Facility Siberian Solar Radio Telescope [http://ckp-rf.ru/usa/73606].

ORCID iDs

Alexandra L. Lysenko @ https://orcid.org/0000-0002-3942-8341

Gregory D. Fleishman @ https://orcid.org/0000-0001-5557-2100

References

Altyntsev, A., Meshalkina, N., Mézárosová, H., et al. 2016, \textit{SoPh}, 291, 445

Altyntsev, A. T., Fleishman, G. D., Lesovoi, S. V., & Meshalkina, N. S. 2012, \textit{ApJ}, 758, 138

Altyntsev, A. T., Fleishman, G. D., Huang, G.-L., & Melnikov, V. F. 2008, \textit{ApJ}, 629, 111

Altyntsev, A. T., Lesovoi, S. V., Meshalkina, N. S., & Yan, Y. 2007, \textit{SoPh}, 242, 111

Atwood, W. B., Abdou, A. A., Ackermann, M., et al. 2009, \textit{ApJ}, 697, 1071

Benka, S. G., & Holman, G. D. 1994, \textit{ApJ}, 435, 469

Benz, A. O. 1986, \textit{SoPh}, 104, 99

Brown, J. C., Conway, A. J., & Aschwanden, M. J. 1998, \textit{ApJ}, 509, 911

Bykov, A. M., & Fleishman, G. D. 2009, \textit{ApJL}, 692, L45

Dennis, B. R., Duval-Poo, M. A., Piana, M., et al. 2018, \textit{ApJ}, 867, 82

Fleishman, G. D., Anfinogentov, S., Loukitcheva, M., Mysh'yakov, I., & Stupishin, A. 2017, \textit{ApJ}, 839, 30

Fleishman, G. D., Bastian, T. S., & Gary, D. E. 2008, \textit{ApJ}, 684, 1433

Fleishman, G. D., Kontar, E. P., Nita, G. M., & Gary, D. E. 2011, \textit{ApJL}, 731, L19

Fleishman, G. D., Kontar, E. P., Nita, G. M., & Gary, D. E. 2013, \textit{ApJ}, 768, 190

Fleishman, G. D., & Kuznetsov, A. A. 2010, \textit{ApJ}, 721, 1127

Gary, D. E., Fleishman, G. D., & Nita, G. M. 2013, \textit{SoPh}, 282, 38

Grady, K. J., Neukirch, T., & Giuliano, P. 2012, \textit{A&A}, 546, A85

Kochanov, A. A., Fleishman, G. D., & Kuznetsov, A. A. 2018, \textit{ApJ}, 867, 84

Kondo, N., Gary, D. E., Wang, H., et al. 2018, \textit{ApJ}, 852, 32

Kurudera, N., Gary, D. E., & Watanabe, S. 2016, \textit{ApJ}, 822, 71

Kurudera, N., Gary, D. E., & Watanabe, S. 2016, \textit{ApJ}, 822, 71

Lemen, J. R., Title, A. M., Akin, D. J., et al. 2012, \textit{SoPh}, 275, 17

Lee, J. W., & Gary, D. E. 1994, \textit{SoPh}, 153, 347

Litvinenko, Y. E. 1996, \textit{SoPh}, 167, 321

Lysenko, A. L., Altyntsev, A. T., Meshalkina, N. S., Zhdanov, D., & Fleishman, G. D. 2018, \textit{ApJ}, 856, 111

Mann, G., Aurass, H., & Warmuth, A. 2006, \textit{A&A}, 454, 969

Meegan, C., Lichti, G., Bhat, P. N., et al. 2009, \textit{ApJ}, 702, 791

Melrose, D. B., & Brown, J. C. 1976, \textit{MNRAS}, 176, 15

Meshalkina, N. S., Altyntsev, A. T., Sych, R. A., Chernov, G. P., & Yihua, Y. 2004, \textit{SoPh}, 221, 85

Milne, D. E., & Sibthorpe, G. 1997, \textit{AAS}, 561, A72

Miller, J. A., & Moore, R. L. 1999, \textit{ApJ}, 520, 445

Nakajima, H., Nishio, M., Enome, S., et al. 2012, \textit{SoPh}, 275, 32

Nakajima, H., Nishio, M., Enome, S., et al. 2012, \textit{SoPh}, 275, 32

Nitta, G. M., Fleishman, G. D., Kuznetsov, A. A., Kontar, E. P., & Gary, D. E. 2015, \textit{ApJ}, 799, 236

Nitta, G. M., Gary, D. E., & Lee, J. 2004, \textit{ApJ}, 605, 528

Petrov, L., & Liu, S. 2004, \textit{ApJ}, 610, 550

Priest, E., & Forbes, T. 2000, Magnetic Reconnection (Cambridge: Cambridge Un. Press), 612

Qin, J., Gary, D. E., & Fleishman, G. D. 2009, \textit{SoPh}, 255, 107

Scherrer, P. H., Schou, J., Bush, R. L., et al. 2012, \textit{SoPh}, 275, 207

Sonof, B. V., & Kosugi, T. 1997, \textit{ApJ}, 485, 859

Sturrock, P. A., Kaufman, P., Moore, R. L., & Smith, D. F. 1984, \textit{SoPh}, 94, 341

Tori, C., Tsukiji, Y., Kobayashi, S., et al. 1979, \textit{PRL}, 26, 129

Trubnikov, B. A. 1965, \textit{RvPP}, 1, 105

Vlahos, L., & Isliker, H. 2019, \textit{PPCF}, 61, 014020

Vlahos, L., Pisokas, T., Isliker, H., Tsilios, V., & Anastasiadis, A. 2016, \textit{ApJL}, 827, L3

Zhelezniakov, V. V. 1969, Radio Emission of the Sun and Planets 1st ed.; Oxford, New York: Pergamon

Zuccarello, F. P., Seaton, D. B., Mierla, M., et al. 2014, \textit{ApJ}, 785, 88