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SAW synthesis with IDTs array and the inverse filter: toward a versatile SAW toolbox for microfluidics and biological applications.

Antoine Riaud, Michael Baudoin, Jean-Louis Thomas, Olivier Bou Matar.

Abstract—Surface acoustic waves (SAWs) are versatile tools to manipulate fluids at small scales for microfluidics and biological applications. A non-exhaustive list of operations that can be performed with SAW includes sessile droplet displacement, atomization, division and merging but also the actuation of fluids embedded in microchannels or the manipulation of suspended particles. However, each of these operations requires a specific design of the wave generation system, the so-called interdigitated transducers (IDTs). Depending on the application, it might indeed be necessary to generate focused or plane, propagating or standing, aligned or shifted waves. Furthermore, the possibilities offered by more complex wave-fields such as acoustical vortices for particle tweezing and liquid twisting cannot be explored with classical IDTs. In this paper, we show that the inverse filter technique coupled with an interdigitated transducers array (IDTA) enables to synthesize all classical wave-fields used in microfluidics and biological applications with a single multifunction platform. It also enables to generate swirling SAWs, whose potential for the on-chip synthesis of tailored acoustical vortex is illustrated on sessile droplets by showing successively droplet atomization of droplets [1], the potential of SAWs for fluid actuation at microscale has been widely explored in the literature: Progressive waves synthesized by straight IDTs enable sessile droplets displacement [2], [3], [4], [5] or fluid pumping in a micro-channel [6], [7]. Acoustic field generated by pairs of IDTs can be combined to synthesize stationary waves and manipulate collectively particles [8], [9], [10], [11], [12], [13], [14], [15], or cells [16], [17], [18], [19], [20], [21], [22] in droplets or embedded in a microfluidic chamber. Focused waves synthesized by concentric IDTs are suitable for the fusion of droplets [23] or for high power applications such as droplet atomization [24]. Finally, more complex operations such as mixing at low Reynolds number through chaotic advection or droplet division may require some fancy combination of plane waves with either rotating [25] or shifted [26] wavefronts. So far, it has thus been demonstrated that SAWs enable to perform many basic operations required in microfluidics and biological applications [27], [28].

Nevertheless each of these operations requires a specific optimized design, which is not compatible with a multi-function actuation platform required for the development of many labs-on-chips. Moreover, classical IDTs do not allow the synthesis of swirling SAWs [29] envisioned for on-chip synthesis of tailored acoustical vortices [30] and consequently three-dimensional single particle manipulation [31] and vorticity control [32]. To overcome these shortcomings, we developed an array of 32 optimized IDTs driven by a programmable electronics that enables independent control of each transducer. To synthesize the targeted wave-field, the inverse filter technique [33] originally developed for bulk waves has been adapted for SAWs [29]. In this paper, we show that it is possible to synthesize plane waves in different directions, focused waves with focal point located at arbitrary position and swirling SAWs with the same device. The potential of this system is illustrated on sessile droplets by showing successively droplet controlled displacement, division, fusion and nebulization with the same platform.

I. INTRODUCTION

Since the seminal work of Shiokawa in 1989 on the atomization of droplets [1], the potential of SAWs for fluid actuation at microscale has been widely explored in the literature: Progressive waves synthesized by straight IDTs enable sessile droplets displacement [2], [3], [4], [5] or fluid pumping in a micro-channel [6], [7]. Acoustic field generated by pairs of IDTs can be combined to synthesize stationary waves and manipulate collectively particles [8], [9], [10], [11], [12], [13], [14], [15], or cells [16], [17], [18], [19], [20], [21], [22] in droplets or embedded in a microfluidic chamber. Focused waves synthesized by concentric IDTs are suitable for the fusion of droplets [23] or for high power applications such as droplet atomization [24]. Finally, more complex operations such as mixing at low Reynolds number through chaotic advection or droplet division may require some fancy combination of plane waves with either rotating [25] or shifted [26] wavefronts. So far, it has thus been demonstrated that SAWs enable to perform many basic operations required in microfluidics and biological applications [27], [28].

Nevertheless each of these operations requires a specific optimized design, which is not compatible with a multi-function actuation platform required for the development of many labs-on-chips. Moreover, classical IDTs do not allow the synthesis of swirling SAWs [29] envisioned for on-chip synthesis of tailored acoustical vortices [30] and consequently three-dimensional single particle manipulation [31] and vorticity control [32]. To overcome these shortcomings, we developed an array of 32 optimized IDTs driven by a programmable electronics that enables independent control of each transducer. To synthesize the targeted wave-field, the inverse filter technique [33] originally developed for bulk waves has been adapted for SAWs [29]. In this paper, we show that it is possible to synthesize plane waves in different directions, focused waves with focal point located at arbitrary position and swirling SAWs with the same device. The potential of this system is illustrated on sessile droplets by showing successively droplet controlled displacement, division, fusion and nebulization with the same platform.

II. METHODS

Rayleigh surface acoustic waves (R-SAWs) are synthesized at the surface of a X-cut, 1.05 mm thick, Niobate Lithium (LiNb03) piezoelectric substrate by an array of 32 unidirectional interdigitated transducers (SPUDT IDTs) (see Fig. 1). The X-cut was chosen for its good electro-mechanical coefficients along Z (\(K^2 = 5.9\%\)) and Y (\(K^2 = 3.1\%\)) directions and its weaker anisotropy compared to the 128° Y-cut generally used for unidirectional IDTs. The IDTs array (IDTA) was fabricated using a lift-off process: (i) the substrate is coated with a AZ15-10 photresist sacrificial layer patterned with conventional photolithography technique, (ii) a titanium (Ti) layer of 20 nm and a gold (Au) layer of 200 nm are deposited by evaporation (titanium is used for its good adherence on LiNb03 and gold for its good electrical conductivity), (iii) the sacrificial layer is washed out by a developer.

The IDTA has been designed for a working frequency of 11.9 MHz, with a wavelength adapted to each wave propagation direction of the anisotropic LiNbO3 crystal. Compared to previous work by the authors [29], the design has been further optimized by placing the IDTs on a slowness curve

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and slightly curving the IDTs to promote diffraction. These two modifications improve the illumination by each transducer of the central zone (radius of 5 mm) of the substrate that we call the "acoustical scene" and where microfluidic operations are performed. An optimal spatial coverage is indeed essential for the synthesis of a wide variety of acoustic wave-fields.

Each of the IDTs is excited independently with a dedicated programmable electronics that enables the synthesis of wave packets at carrying frequencies up to 12 MHz. Impedance matching for each transducer was achieved with external electronic components (inductances). Finally, the inverse filter method \[33\] was used to determine the optimal input signal for each IDT to synthesize a targeted wave-field. Indeed, the inverse filter is a very general method to synthesize a specific wave-field in a linear medium given a set of independent programmable sources. This process can be basically decomposed into three distinct stages. First, the signal emitted by each transducer (impulse response) is measured in the acoustics scene. In practice this response is recorded in a number of control points whose distance cannot exceed $\lambda/2$ according to Nyquist-Shannon sampling principle. This allows to define, in the Fourier space, a transfer matrix $H_{ij}(\omega)$ (called the propagation operator) between the Fourier transform of the entrance signal emitted by transducer $j$, $E_j(\omega)$, and the response signal at control point $i$, $S_i(\omega)$: $S_i = H_{ij}E_j$ (with Einstein notations). In the present experiments, the surface vibrations of the substrate at control point $i$ (typically of the order of a few nanometers) are measured by a homemade polarized Michelson interferometer whose principle is given in reference \[29\]. Then, the targeted output signal $S$ is defined and the transfer matrix $H$ is inverted to compute the optimal input signal $E = H^{-1}S$. Finally, the optimal signal is synthesized by each transducer. If $e_j(t)$, $s_i(t)$ and $h_{ij}(t)$ are the inverse Fourier transform of $E_j(\omega)$, $S_i(\omega)$ and $H_{ij}(\omega)$, it is worth noting that the output time signal $s(t)$ is the convolution product of $h_{ij}(t)$ and $e_j(t)$:

$$s_i(t) = h_{ij}(t) \ast e_j(t).$$

While the inverse filter method is simple in principle, some complexity arises when implementing it. Indeed, the propagation operator is generally ill-conditioned since small errors in the measurements produce very large errors in the reconstructed results. Then, the number of control points is not necessarily the same as the number of sources (transducers) and thus the propagation operator is not necessarily a square matrix. So, the pseudo-inverse of the propagation operator is obtained through singular value decomposition. Finally, the inverse filter technique had been initially developed to generate acoustical wave-fields in 3D media. In this case, the target field is a surface and has a smaller dimensionality (2D) than the propagative medium (3D), whereas for SAWs the target field has the same dimensionality as the propagative medium (both 2D). So the control points are not independent and the wave-field must fulfill the dispersion relation. This requires some refinements in the method (see Ref. \[29\]).

To enable droplet manipulation, the central zone was treated with a hydrophobic self assembled monolayer. Otherwise, the droplet would spread on the gold layer at the center of the Niobate Lithium substrate since it is a perfectly wetting medium. Nevertheless, the adherence of alkane-thiol molecules on the central gold layer was not optimal leading to contact angle below 90° ($\theta \approx 70°$), large hysteresis and thus pining of the contact line. Despite these bad properties of the hydrophobic layer, we nevertheless succeeded to control the drop displacement with the IDTA as we will see in the next section. The droplet dynamics was recorded with a Flea 3 camera on a MZ1 macroscope at 75 frames per second. A sketch of the experimental setup is shown on Fig. 2.

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**Fig. 1.** Optimized array of 32 interdigitated unidirectional transducers used for the synthesis of various surface acoustic wave-fields (focused, plane, swirling) and the manipulation (displacement, division, fusion, atomization) of droplets. The central black zone is a gold layer used as a mirror for the measurement of the transducer response with the Michelson interferometer.

**Fig. 2.** Sketch of the experimental setup used for the synthesis of various wave-fields and the actuation of droplets.
III. RESULTS

A. Complex wave-fields synthesis

To demonstrate the potential of the SAW toolbox for fluid samples actuation, we first investigated the possibilities offered by the IDTA and the inverse filter technique to synthesize the main surface acoustic wave-fields used in the literature: plane, focalized and swirling SAWs.

While our setup is optimized for the synthesis of focalized waves and swirling SAWs (since the IDTs are disposed radially around the slowness curve), we have shown that it is possible to synthesize waves with plane wavefronts in the desired direction with peak to peak amplitudes larger than 5.5 nm, that is to say well above the values classically used for droplets displacement [4], [5]. We provide on Fig. 3 two examples of plane progressive waves synthesized in different directions. These results show that despite the curvature of the IDTs, the wavefront aberration is weak in the acoustical scene and compensated by the inverse filter.

Then, we synthesized focalized waves with different positions of the focal point in the acoustical scene and apodization around a preferential direction φ₀ (see Fig. 4). It is important to note that contrarily to previous attempts to synthesize focalized waves for microfluidic applications with concentric IDTs [27], the anisotropy of the piezoelectric medium is considered here in the definition of the targeted wave-field:

\[ F(r, \theta) = \frac{1}{2\pi} \int_{-\pi}^{\pi} h(\phi - \phi_0, \sigma) e^{ik_r(\phi)r \cos(\phi - \phi_0)} d\phi, \]

with \( h(\phi - \phi_0, \sigma) = \exp \left( -\frac{||\phi - \phi_0||^2}{4\pi^2\sigma^2} \right) \),

\((r, \theta)\) the polar coordinates, \( k_r(\phi) = \omega/c_R(\phi) \), the radial wave vector, \( c_R(\phi) \), the phase speed of R-SAWs in the \( \phi \) direction (defining the anisotropy of the medium), \( \sigma \) the aperture (here \( \sigma^2 = 0.2 \)) and the symbol \( || \) denotes the shorter angular distance (which can be computed as follows \( ||\phi - \phi_0|| = \arccos(\cos(\phi - \phi_0)) \)). The function \( h \) then represents an apodization over an aperture \( \sigma \).

Consideration of the anisotropy is indeed essential to ensure real focalization of the acoustic wave. Excellent results are obtained (see Fig. 4) with maximum normal amplitude of the R-SAW of up to 100 nm. Naturally, small discrepancies are observed compared to the targeted wave-field (the phase does not exactly follows the slowness curve) owing (i) to the finite numbers of transducers used for the field synthesis and (ii) to the finite number of measurement points obtained with the interferometer and used for the reconstruction of the experimental acoustic field.

Finally, anisotropic swirling SAWs of topological order 0 and 2 have been synthesized with the new transducers array presented in this paper (see Fig. 5). The targeted wave-field is defined according to the formula introduced in ref. [29]:

\[ W_l(r, \theta) = \frac{1}{2\pi^2} \int_{-\pi}^{\pi} e^{il\phi + ik_r(\phi)r \cos(\phi - \phi_0)} d\phi, \]

with \( l \) the topological order of the swirling SAW. It is interesting to note that swirling SAWs of order 0 are nothing but focalized waves with no angular apodization. These waves are not appropriate for particles tweezing or vorticity control since they do not have phase singularity (and thus dark spot) at their center to trap particles and they do not carry angular momentum contrarily to higher order swirling SAWs. Nevertheless, they can be of much practical use for applications where high intensity is required at the focal point.

B. Droplet manipulation with the platform

These specific wave-fields have been used to perform operations on water droplets of initial volume 2 μl. Since it is not possible to synthesize continuous wave-fields with the programmable electronics, some burst of duration 25 μs, carrying frequency 11.9 MHz and variable repetition rates of
Fig. 5. Phase and amplitude of anisotropic swirling SAWs of topological order 0 and 2 (a and b). The maximum peak to peak amplitude of the $W_0$ and $W_2$ swirling SAWs are respectively 108 nm and 80 nm. Colorbar: peak to peak amplitude $\times 10^{-2}$ nm.

Fig. 6. Stack of images showing the displacement forward and backward of a 2 $\mu$l droplet in the acoustical scene. The displacement is obtained with focalized waves propagating successively in the opposite directions. The time elapsed between two successive images is 53 ms. See also movie S1.

Fig. 7. Stack of images showing the fusion of two droplets of 2 $\mu$l. The fusion is obtained with a centered swirling SAWs of topological order 2. The time elapsed between two successive images is 27 ms. See also movie S3.

Fig. 8. Stack of images showing the atomization (nebulization) of a 2 $\mu$l droplet. It is obtained with a high intensity centered swirling SAW of order 0 (annular wave). The time elapsed between two successive images is 13 ms. See also second part of movie S3.

a few kHz have been used for droplet actuation (for each operation, the exact sequence used for actuation is described on the corresponding figure). Since droplet displacement is the result of cumulative nonlinear effects (radiation pressure and acoustic streaming), and the characteristic hydrodynamic times associated with droplets motion are slow compared to the repetition rates, the forcing is essentially seen as a continuous forcing. Nevertheless, the repetition rates of several kHz are compatible with droplets high order inertio-capillary vibrations [34], [35], [5], [36], which may explain why spurious atomization of the drop has been observed. Indeed, both the frequency of the excitation and the acoustical powers used in the present experiments are compatible with droplet nebulization [35] (larger power than usual were used in the present experiments to overcome the retention of the contact line). Nevertheless, this shortcoming could be simply overcome with appropriate hydrophobic treatment of the surface with low hysteresis [37].

Droplet displacement (Fig. 6, Movie S1), fusion (Fig. 7, movie S3) and atomization (Fig. 8, second part of movie S3) were obtained respectively with focalized waves, swirling SAWs of second and zero order. The characteristic of the wave-field are summarized on the corresponding figure. For the droplet division (Fig. 9, movie S2), we used a different method than the one proposed in ref. [26]: we alternatively
synthesized some burst of focalized waves with two different focal points as presented in the previous subsection. With this specific wave-field, we were able to separate droplets even at these high contact line hysteresis.

![Stack of images showing the asymmetric division of a 2 µl droplet into two daughter droplets of different volumes.](image)

**Fig. 9.** Stack of images showing the asymmetric division of a 2 µl droplet into two daughter droplets of different volumes. It is obtained with waves focalized at two focal points situated on both sides of the drops and with angular apodization. The time elapsed between two successive images is 27 ms. See also movie S2.

### IV. DISCUSSION

In this paper, we have shown that the combination of interdigitated transducers array (IDTA) and the inverse filter technique enables the synthesis of the most common surface acoustic wave-fields used for actuation of fluids at the microscale: plane waves in different directions, anisotropic focalized SAWs and anistropic swirling SAWs. As a proof of concept, we show that this SAW toolbox enables to perform many basic operations required in droplet based digital microfluidics: droplet displacement, division, fusion and atomization. Since it is virtually possible to synthesize any acoustic wave-field compatible with the anisotropy of the substrate, it might be easily demonstrated that it is possible to perform other operations previously demonstrated in the literature such as micro-mixing, collective particle manipulation with standing waves, or jetting. In the same way, it might be possible to demonstrate the versatility of this platform for fluid samples manipulations in microchannels.

The most thrilling perspectives of this SAW toolbox nevertheless lie in the development of new operations that cannot be achieved with other techniques, such as selective 3D manipulation of one or a few particles or cells (displacement, rotation), precise vorticity control independently of the boundary conditions with swirling SAWs, or collective manipulation of several sessile droplets. This last operation is indeed not possible with a limited number of transducers since (i) there is a shadow zone behind each droplet that prevents the displacement of a second droplet situated behind it due to the strong absorption of Rayleigh waves by liquid samples, and (ii) it would be necessary to localize the droplets position in real time. This problems can be overcome with IDTA. Indeed, the combination of the acoustic waves emitted by each transducers would enable better spatial coverage of the substrate and thus the elimination of shadows zone. Moreover the IDTs can be used not only as actuators but also as sensors of the acoustical echo as demonstrated by Alzuaga et al. [38], [39] and Renaudin et al. [40] to determine the location of the drop without extra visualization setup.

This work opens prospects toward the design of potentially the most versatile toolbox for active control of small fluid samples, for microfluidics and biological applications.

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