Crystal Engineering in Continuous Plug-Flow Crystallizers

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Supporting Information

ABSTRACT: Size, shape, and polymorphic form are the critical attributes of crystalline particles and represent the major focus of today’s crystallization process design. This work demonstrates how crystal properties can be tuned efficiently in solution via a tubular crystallizer that facilitates rapid temperature cycling. Controlled crystal growth, dissolution, and secondary nucleation allow a precise control of the crystal size and shape distribution, as well as polymorphic composition. Tubular crystallizers utilizing segmented flow such as the one presented in our work can provide plug flow characteristics, fast heating and cooling, allowing for rapid changes of the supersaturation. This makes them superior for crystal engineering over common crystallizers. Characterization of particle transport, however, revealed that careful selection of process parameters, such as tubing diameter, flow rates, solvents, etc., is crucial to achieve the full benefits of such reactors.

1. INTRODUCTION

Crystal engineering involves the ability to specifically tune the physicochemical properties of crystalline matter. As such, crystal engineering is based on an understanding of intermolecular interactions in the context of crystal packing and the utilization of such understanding in the design of new solids with desired physical and chemical properties.1 This involves the arrangement of the atoms or molecules that comprise the crystal, as well as the size and morphology of individual crystals. While the lattice structure and associated defects determine a crystal’s thermodynamic properties, the macromolecular properties such as shape determine the kinetic effects.

Pharmaceutical applications typically involve organic crystals of small molecules with a molecular weight <500 g/mol that can crystallize in several polymorphic forms, i.e., the same molecule(s) arranged in a different crystal lattice. Most new drugs on the market and in the development pipelines fall into class II biopharmaceuticals, and as such, exhibit a high permeability but low solubility. The low solubility poses significant challenges for drug release.2 While the solubility depends on the crystal structure (with amorphous forms usually providing the highest solubility), the dissolution rate is also affected by the total crystal surface area. The surface energy of a crystal is face-specific.3,4 Therefore, the crystal shape also affects the dissolution kinetics.5 This highlights the importance of the intra- and macromolecular properties of crystalline matter for a drug’s bioavailability. Furthermore, crystal properties play a key role in pharmaceutical process development and production. Crystal size and shape determine the design of downstream operations, such as filtration, drying washing, mixing, tableting, capsule filling, and powder flow properties in general. Different crystal facets expose the molecules at different orientations which can influence a wide range of properties such as catalytic activity, the tendency for electrostatic charging, wettability, hydrophobicity, and chemical stability.6–9 Therefore, crystal shape engineering can improve the long-term stability and extend the shelf life of crystalline pharmaceuticals. It should be pointed out that size and shape of crystalline matter are always distributions, which will affect the use of this particulate system dramatically.

Crystallization from solution is the prevailing process for separation and purification in pharmaceutical manufacturing. Tuning the crystals’ physiochemical properties at this stage allows to define the product crystals’ attributes at the beginning of the production.

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A common approach to crystal engineering in solution involves the use of additives. However, an addition of chemicals might require further separation steps and poses additional regulatory and quality control challenges for pharmaceutical production. An alternative approach is supersaturation control, which provides a nonchemical route to change crystal properties during the crystallization process, or directly after, while the crystals are still in solution. Tight supersaturation control is not trivial, and traditional batch crystallizers quickly reach their operational limits, if high supersaturation levels and rapid changes of the latter are required.

Tubular crystallizers (typically with an inner diameter of <10 cm and a length >1 m) are characterized by a high surface-to-volume ratio which facilitates faster heat transfer than in equivalent batch reactors.

As the tube diameter gets smaller, the heat transfer rates increase. Tubular crystallizers are suitable for continuous operations and have successfully been applied to a wide range of applications for crystallization from solution.

What these crystallizer designs have in common is that supersaturation is controlled via a predefined temperature trajectory along the flow direction. However, processing solid particles in small channels is challenging and becomes impossible as the tube diameter approaches the size of manufactured crystals. Depending on the process conditions, fouling or localized accumulations can result in clogging the reactor. Better particle dispersion and plug flow characteristics for the solid phase can be achieved via segmented flow, i.e., by feeding a gas or an immiscible liquid phase.

The latter is less common in crystallization due the limited number of green nonpolar solvents of appropriate viscosity and miscibility. In addition, heating rates are reduced due to an additional heat capacity of the second fluid and the (generally) thicker wall film. Moreover, phase separation is required downstream.

In this work we demonstrate that a tubular crystallizer, operated in gas–liquid segmented flow mode, can carry out three important crystal-engineering processes continuously, and within minutes, by rapid changes of the supersaturation. First, particle transport in gas liquid segmented flows is discussed, followed by three sections on (i) the removal of fine crystals, (ii) the tuning of crystal shapes, and (iii) the transition between polymorphic forms. Other particle engineering challenges, including the engineering of the solvates/hydrate form or amorphous–crystalline transformations, can be addressed as well and will be the focus of future work.

2. PARTICLE TRANSPORT IN GAS–LIQUID SEGMENTED FLOW

As the tubing diameter decreases, surface tension forces become more relevant in multiphase flows, leading to various flow patterns depending on the gas- and liquid-flow rates as shown in Figure 1. At low gas flow rates, relative to the liquid phase, bubbles appear in the reactor; i.e., bubbly flow is observed. An increase in the gas flow rates leads to segmented flow (also referred to as gas–liquid Taylor flow or bubble train), which consists of elongated bubbles that can be many times longer than the channel diameter. At high gas-flow rates, annular flow is observed. If both liquid and gas flow rates are high, highly turbulent churn flow can occur. Besides the relative flow rates, the occurrence of a specific flow pattern depends on the fluid properties (e.g., viscosity μ and surface tension σ) affecting the liquid’s behavior on the tube walls, and on the dimensions of the channel and junction.

Since the 1960s, several groups have been able to successfully predict the flow patterns via flow maps using dimensionless parameters. However, most flow maps are applicable only close to the conditions for which they were obtained. For stable gas–liquid flow at flow rates >1 mL/min capillaries with an inner diameter of <1 cm are required. Thus, tubing of d_{in} = 2 mm was chosen for this study to process crystals between 1 and 500 μm in segmented flow.

In gas–liquid segmented flows, heat and mass transfer, as well as particle transport in the slugs, is determined by a wetting film adjacent to the tubing wall (Figure 1). This phenomenon has been extensively studied, and several expressions correlating film thickness to the channel diameter d and the Capillary number Ca (= μν/σ) have been proposed. The film thickness increases with Ca, i.e., with increasing flow rates/liquid velocities ν. The effect of gravity on the film thickness is negligible, especially at small values of Ca < 10^4 but cannot be neglected for particle transport. The relative magnitudes of gravity, buoyancy, and drag forces determine if particles are suspended homogeneously within a slug or if they accumulate in the rear of the slug.

To demonstrate how particle transport in a gas–liquid segmented flow is determined by the flow and particle properties, a β-mannitol suspension was pumped through a d_{in} = 2 mm tubing and monitored via a high-speed camera. 2.1. Materials and Methods: Particle Transport in Small Tubing. Three sieved fractions of β-mannitol (non-commercial sample of high α-form content, spray-dried type, Roquette, France) were suspended in a saturated solution of 60% ethanol (ethanol: 99.8%, denaturized, Carl Roth GmbH, Germany) and 40% water (w/w) or saturated water. The size fractions were large (150–180 μm), medium (90–150 μm), and small (50–80 μm). The solid mass fraction was 0.1 g/100 g of solution. The suspension was pumped through a tubing of 10 m with a peristaltic pump at various flow rates, V_{Susp}. We used polysiloxane tubing (Versilic, Saint Gobain, France) with an inner diameter d_{in} of 2.0 mm and an outer diameter (d_{out}) of 4.0 mm. The segmented flow was generated by injecting air via a syringe pump using a T-fitting. The ratio of suspension-to-gas flow rates was fixed to V_{Susp}/V_{Air} = 1.6. After 1 m the tube was passing the field of view of a high-speed camera recording...
at a frame rate of 500 fps, as described by us recently\textsuperscript{21} and as illustrated in Figure S1.

2.2. Results and Discussion: Particle Transport in Small Tubing. Images taken from the videos (all available for download in the Supporting Information) are shown in Figure 2. They highlight the influence of the flow rate and particle size on the dispersion of particles in the segments. Only at the highest flow rate ($V_{\text{tot}} = 18.7 \text{ mL/min}$), the large D-mannitol crystals were dispersed throughout the slug, although not homogeneously. Low ($V_{\text{tot}} = 8.7 \text{ mL/min}$) and moderate ($V_{\text{tot}} = 13.7 \text{ mL/min}$) flow rates caused accumulation of crystals in the lower part of the slug. Moreover, crystals accumulated at the rear end of theslug at the lowest flow rate. Also, medium-sized crystals spread more homogeneously at the highest flow rate, yet they were not perfectly dispersed throughout the segments. For low and intermediate flow rates, the particle concentration was higher in the lower vortex, but no accumulation in the rear end was observed even at the lowest flow rate. The smallest crystals were suspended almost homogeneously at the moderate flow rate. However, accumulation at the bottom was still observed even at the lowest flow rate. In this context, accumulation should not be confused with sedimentation, i.e., crystals trapped in the wall film at the bottom of the slug that are not recirculated.

Yet, the results indicate that increasing the flow rates is an obvious choice for improving the dispersion of particles in the liquid segments separated by gas.

However, not only the flow rates impact the dispersion of particles, but also the wall film thickness increases with the increase in flow rates, as discussed above. The wall film thickness $\delta_{\text{film}}$ can be calculated using well-known semiempirical expressions, summarized in ref \textsuperscript{30}. The range of wall thickness calculated via these expressions is shown for every case in Figure 2. A surface tension of $\sigma_{\text{EthOH}} = 25.26 \times 10^{-3} \text{ N/m}$ was identified, based on the contact angle measurements. Surface tension data of all liquid phases in this study are presented in the Supporting Information, Table S1. Crystals can pass from one slug to another via the wall film (see Figure 1) if sedimented crystals are of similar or smaller size compared to the film thickness. As the film thickness increases at higher flow rates, larger crystals might travel between slugs, despite the improved dispersion. The images in Figure 2 (and the related videos) show that medium and especially small D-mannitol crystals can travel between neighboring slugs if they become trapped in the wall film at the bottom. The consequence is a broader residence time distribution (RSD) of particles. Hence, deviations from an ideal plug flow reactor were strongest for the small D-mannitol crystals, with a considerable number of crystals passing through the wall film. In contrast, the largest D-mannitol crystals remained in the original slug and did not pass through the liquid wall film for all studied flow rates. Thus, a very narrow RSD of the particulate phase in the tube is obtained, although the large particles were not dispersed homogeneously within each segment.

In summary, an increase in flow rate can improve particle dispersion within the segments but comes along with an increase in wall film thickness. This might allow larger particles to travel between slugs. In order to achieve ideal plug flow characteristics for the particulate phase, the film thickness should be significantly smaller than the particle diameter. This can be addressed for example by the solvent selection. Using pure water as a solvent significantly improves particle transport (minimizing/avoiding crystals passing through the liquid wall film) compared to ethanolic solutions. Because of its high surface tension $\sigma_{\text{H}_2\text{O}} \approx 70 \times 10^{-3} \text{ N/m}$, the liquid wall film thickness is reduced significantly, e.g., $\sim 50\%$ compared to the 60% ethanolic solution used for this study. As a consequence,
sedimentation of small crystals could be avoided using pure water as shown in Figure S2a.

Apart from an increase in the total flow rate, particle dispersion can also be improved by reducing the length of the liquid segments, e.g., by decreasing the ratio of $V_{\text{Susp}}/V_{\text{Air}}$ as shown in Figure S2b. In addition, an increase in the density of the liquid allows for a better dispersion as demonstrated in the Supporting Information providing additional videos of glass beads and sand dispersed in various solvents differing in density.

3. FINES REMOVAL

As reported by several groups,\textsuperscript{49–56} temperature cycling via single or multiple cycles is a simple, yet effective, procedure for tuning the crystal size distribution (CSD) and eliminating fines. Tubular crystallizers operated in segmented flow mode offer several advantages for temperature-cycling. They allow for sharp residence time distributions of the crystals in each stage of the reactor if operated properly (section 2), and facilitate particle dispersion at minimum agitation. This minimizes crystal collisions and hence possible aggregation or agglomeration events during the cooling stages, i.e., where the suspension is supersaturated. Agitation is also well-known to reduce the induction time for primary\textsuperscript{57} and secondary\textsuperscript{58} nucleation. Furthermore, there are no moving parts (e.g., stirrers) that could lead to attrition.

The concept of fines removal via subsequent heating and cooling cycles is as follows: a temporary increase in the temperature causes an overall decrease in the crystal size due to dissolution, with the smallest particles disappearing completely. The subsequent cooling stage(s) introduce(s) recrystallization, allowing the remaining crystals to grow back to their initial size and larger (assuming no new nuclei are formed).\textsuperscript{49,51} Consequently, the CSD is shifted toward larger crystals. If fines cannot be removed within a single temperature cycle, the maximum temperature can be increased. However, excessive dissolution needs to be avoided due to the high supersaturation levels during the successive cooling stage and the low surface area of remaining crystals. This makes the process slow and requires the temperature difference to be adjusted each time the size of the initial crystals change. Whether multiple temperature cycles are superior to a single temperature cycle to remove fines is determined by the size dependence of the crystal growth and dissolution rates. If the growth and dissolution rates are independent of the crystal size, the CSD does not change with more than one cycle. This is demonstrated in Figure 3 showing in silico results (of a population balance model) how multiple temperature cycles influence the CSD in the case of size-independent and size-dependent growth rate. Details of the population balance model are shown in the Supporting Information, section SI 3. Such population balance equation models have been used by several groups to understand the effect of cycling on the CSD and the crystal shape.\textsuperscript{59–62}

Many systems show a clear size dependence of growth or dissolution rates, which is why most experimental and computational studies conclude that effective elimination of fines or efficient tuning of CSD cannot be achieved within a single cycle. Reasons for this size dependence are discussed, for example, in refs 63–66. Hence, multiple cycles allow for significant changes in the CSD. The same effect, i.e., a continuous change in the CSD with more cycles, is also expected for growth rate dispersion (different crystals of the same size exhibit different growth or dissolution rates) which is sometimes mixed up with size-dependent growth or dissolution kinetics.

Here we demonstrate effective removal of fines from a commercial D-mannitol sample via the tubular crystallizer using multiple temperature cycles. Because of the fast heating and cooling rates high values of supersaturation could be achieved temporarily at a time scale way below the induction times, i.e., in the absence of primary or secondary nucleation events, allowing distinct changes in CSD within minutes.

3.1. Materials and Methods: Fines Removal from a Commercial D-Mannitol Sample. The D-mannitol powder used in our study (Pearlitol 160C, Roquette, France, used as received) has a broad CSD. The starting suspension was prepared by dispersing the D-mannitol powder (0.3 g per 100 g) in 500 mL of a saturated ethanolic (50% ethanol 50% water) solution (w/w) in a 1000 mL round-bottom flask. Solubility data in the used solvent mixture were determined as described in the Supporting Information, section S5. The flask was briefly immersed in an ultrasonic bath to homogeneously disperse particles and separate aggregates formed during storage. The starting suspension was continuously stirred at 22.0 °C with a magnetic stirrer during the process. The stirrer bar and its speed of rotation were carefully selected to avoid the cone effect, i.e., sedimentation of larger particles in the bottom region, resulting in accumulation of larger particles in the flask when withdrawing from the suspension. The test measurements
Maximum curvature of compartmentalization is achieved by introducing air bubbles via a syringe pump (2 of the 3 of the crystallizer passing the camera. Pumping clear saturated solutions through the tubular tubing, respective experiment. The tubular crystallizer (polysiloxane temperature di ff erences of 2, 4, or 6 °C, depending on the respective experiment. The tubular crystallizer (polysiloxane tubing, 2 mm) comprised 15 loops of 186 cm. In each loop, the suspension was heated at fi rst with the tube immersed in a warm bath (47 cm; 24/26/28 °C), and subsequently cooled in the cooling water bath (113 cm, 22 °C = room temperature). 2 × 13 cm of tubing per loop were used for crossovers from one bath to the other (room temperature = temperature of cooling bath). The unequal partitioning of the tube between the two water baths was used since the dissolution of crystals was expected to be faster than their growth. One meter of tubing was added before the inlet and after the outlet of the reactor. Thus, the total length of the tubular crystallizer was 30 m.

Suspension and air fl ow rates were set to $V_{susp} = 8.5$ mL/min and $V_{air} = 5.2$ mL/min, respectively (i.e., moderate fl ow rates according to section 2). For all settings, initial tests were performed to ensure the absence of primary nucleation by pumping clear saturated solutions through the tubular crystallizer passing the camera.

In order to quantify the changes in the fines content, the CSD was measured immediately. Instead of (error-prone) off line analysis, online laser diffraction was utilized (HELOS, Sympatec GmbH, Germany equipped with a LIXELL fl ow cell). The product suspension, i.e., the suspension exiting the tubing, was fed into a round 30 mL bottomed fl ask kept at 22 °C via a thermostatic bath to remove the gas phase before passing the suspension through a fl ow cell (measurement duration: 15 s, measuring range of size: 4.5–800 μm), see Figure 4, path A.

To compare the multiple-cycles process to a single-cycle one, additional batch experiments were performed. For the batch experiments, the starting suspension was prepared as described above and heated at 0.1 °C/min, i.e., considerably slower than via the tubular crystallizer due to the smaller heat transfer rate in batch, to a temperature of 22.5 °C or 23 °C at which it was kept for 3 min before being cooled to the initial temperature of 22.0 °C at 0.1 °C/min. Higher temperatures were not possible due to complete dissolution. The suspension was analyzed immediately after the cycle via laser diffraction as described above.

3.2. Results and Discussion: Fines Removal from a Commercial d-Mannitol Sample. Figure 5 (top) shows the CSD of the starting suspension compared to products after temperature cycling in the tubular crystallizer at temperature differences of 2 °C, 4 °C, and 6 °C. Respective microscope pictures of the product crystals can be found in Figure 6. Clearly, with an increasing temperature difference the number of fines decreases. Simultaneously, particles of more than 400 μm appear in the product. Because of the fast cycling, <45 s per cycle, the suspension was not in equilibrium at the end of each cycle, i.e., $S \neq 1$ (supersaturation is de fl ned as the ratio of concentration and
solubility, $S = c(w/w)/c^*(w/w)$, throughout this work). The temperature profile was calculated using the model described in the Supporting Information (sections S3 and 6), yielding minimum and maximum temperatures of $T_{\text{min}} = 22.1 \, ^\circ\text{C}$ and $T_{\text{max}} = 24.9 \, ^\circ\text{C}$ (see Figure S13). This $T_{\text{max}}$ corresponds to an undersaturation of $S_{\text{min}} = 0.87$. Rapid temperature cycling in the tubular reactor allowed for high average super- and undersaturations, $\frac{1}{t_{\text{end}} - t_{\text{start}}} \int_{t_{\text{start}}}^{t_{\text{end}}} |S(t)| \, dt \gg 1$, enhancing dissolution and growth.

These high average super- and undersaturations facilitated a more significant change in the CSD via rapid temperature cycling in the tubular crystallizer than via a single temperature cycle performed in batch (see Figure 5, bottom) within shorter time. Tubular crystallizer: 15 cycles, 11 min; batch: 1 cycle, 13 or 23 min). However, fines removal considering the achieved minimal crystal size after cycling was only superior to batch, if the temperature differences exceeded $\Delta T = 2 \, ^\circ\text{C}$.

4. CRYSTAL SHAPE TUNING

Controlling crystal shape is commonly achieved via the addition of growth inhibitors. The face-selective adsorption of these additives decelerates or even blocks growth of the specific facets to control the crystal shape. However, additives increase costs and may add to the complexity of the process. Additives are frequently toxic and require further downstream processes, such as recrystallization and separation. Furthermore, the solvent can influence the integration of solute molecules into the crystal surface, and hence, the crystal shape. This effect is particularly pronounced if the chemical structure of the solvent and the solute are related. The molecular conformation, solvation, and clustering of the solute is also affected by the solvent. However, the occurrence and stability of polymorphic forms do strongly depend on the solvent, which

Figure 5. Measured crystal size distributions of the D-mannitol suspension cycled (top) multiple times via the tubular crystallizer and (bottom) once in batch.

Figure 6. Microscope pictures of product crystals after passing through the tubular crystallizer for different temperature gradients. (a) $\Delta T = 0 \, ^\circ\text{C}$ (constant temperature in both baths, i.e., 22 $^\circ\text{C}$). (b) $\Delta T = 2 \, ^\circ\text{C}$. (c) $\Delta T = 4 \, ^\circ\text{C}$. (d) $\Delta T = 6 \, ^\circ\text{C}$. 
is one reason for the usually very limited number of suitable solvent candidates.

Yet, one more strategy for engineering the shape involves manipulation of the supersaturation, for example, by temperature cycling of the slurry. Employing adequate saturation control in batch processes is known as a simple and highly effective method to control crystal size. Only recently, attempts have been made to influence not only the size, but also the shape of crystals via this approach. Still, most studies on crystal shape tuning are of theoretical nature. Limitations of analytical tools to quantify the multidimensional shape of microcrystals have been recognized as a major bottleneck in controlling the crystal shape. However, recent advances in 2D-image particle analysis allow the study of 3D crystal shapes. All these studies demonstrate that the morphology of a growing crystal evolves toward a steady-state. In contrast, dissolving crystals do not evolve toward such a steady-state. Hence, a crystals shape after multiple dissolution and recrystallization cycles is the combination of the stable steady-state and the nonsteady dynamic dissolution morphology. This explains why a considerable change in crystal shape, i.e., a change in the relative surface area of the crystal facets sufficient to shift the physiochemical properties, many temperature cycles. Each of these, with significant dissolution during the heating stage. As such, crystal shape control via temperature cycling usually requires long process duration, which makes it frequently impractical.

In the current study, we present how the crystal shape of acetylsalicylic acid (a model substance commonly used for shape control studies) can be changed within minutes using a tubular crystallizer. Its ability to go from a dissolution stage at low undersaturation to a growth stage and then reverse this process within seconds allows for significant dissolution in a minimum amount of time without dissolving entire crystals.

4.1. Materials and Methods: Shape Tuning of Acetylsalicylic Acid Crystals. The starting material for shape-tuning experiments was obtained from the commercial acetylsalicylic acid (ASA) powder (ASA 3020, G.L. Pharma, Lannach, Austria) by sieving a fraction of 200–250 μm (size refers to mesh size). Crystals of this size were rather uniform in shape, i.e., rods with a maximum length between 500 and 800 μm (see Figure 6a). In all ASA shape-tuning experiments, a saturated 96% ethanol solution (ethanol: 96%, denaturized, Carl Roth GmbH, Germany) was used. A solid mass fraction of 0.5 g of powder per 100 g of solution was chosen, not to have more than five crystals per segment. This was done to prevent accumulation at the rear ends of the segments which is likely to occur at such slow flow rates (see section 2: moderate flow rates) and can promote aggregation. Since the crystals sizes were considerably larger than the wall film thickness, ideal plug flow characteristics were achieved for the cycled crystals (see section 2).

The tubular crystallizer was designed and operated using the flow rates and unequal partitioning of the tube length as described in section 3.1. In addition, experiments were performed with an equal partitioning, i.e., 80 cm of tubing in the warm and cold bath. A process schematic is shown in Figure 4, path B. Experiments were performed using 5, 10, and 15 cycles. The technical limit of the number of cycles or tube length depends on the maximum pressure the pumps can provide and the pressure drop of the used tube. With the described setup, there were no technical difficulties even when using longer tubing of up to 40 m (data not shown).

The process settings and information about concentration and supersaturation along the temperature cycler are provided in Table 1. The supersaturation values refer to an immediate change in temperature, not considering changes in concentration due to dissolution or growth. The solubility data for ASA were obtained from our previous studies. Temperatures in the water baths were chosen based on high-speed camera videos, monitoring the inlet and outlet, see Figure 7a. The images allowed an initial estimation of successful shape tuning and the absence of nucleation events. The absence of primary nucleation was also tested by cycling a crystal free solution
saturated at 22 °C. Crystals were filtrated right after the outlet for further analysis.

4.2. Results and Discussion: Shape Tuning of Acetylsalicylic Acid Crystals. Figure 7b,c shows micrographs comparing the rod-like ASA feed and the product crystals, i.e., those after temperature cycling in ethanol. A change in the shape was apparent already after five cycles (3.5 min residence time). The surface roughness decreased significantly, and the crystals lost their round shape and became rectangular and plate-like.

This effect was clearly enhanced after 10 cycles and became even more pronounced after 15 cycles showing a significant change in shape. Experiments with the unequal partitioning of the tubing (47 cm cold, 113 cm warm basin) showed a more efficient change of the crystal shape at the same number of temperature cycles.

In a typical batch processes, grinding effects by the stirrer can lead to a decrease in aspect ratio due to smoothening of elongated particles. In our experiments, product crystal shape was not affected by any moving parts. Plate-like crystals were obtained and no abrasion was observed, resulting in a narrow CSD and well-defined crystals. The described tubular crystallizer design, with each temperature cycle lasting <1 min, allows facile control of the crystal shape by increasing or reducing the number of cycles.

5. POLYMORPHISM CONTROL

Following Ostwald’s rule of stages, the rate of nucleation of a metastable form is higher than that of the stable form. However, the polymorphic form with the fastest growth rate (which depends on the material, but is frequently the most stable polymorph) will eventually prevail regardless of the rate of primary or secondary nucleation. In addition, kinetic nucleation theory indicates that the primary nucleation rate of a metastable form is never the highest over the entire supersaturation range.78,79 Thus, the occurrence of a specific polymorph after crystallization is largely determined by its nucleation and growth kinetics in competition with other polymorphic forms. Conversion between polymorphs can occur during various processes and even during handling of the dry powder (e.g., milling). Polymorphic conversion may take anywhere between seconds and decades, making the control of the specific polymorph an important quality parameter of manufacturing.

The conversion of a metastable into the most stable form in solution is likely to follow via a solvent-mediated (polymorphic) transformation (SMT).80,81 This is a reliable route for obtaining the most stable polymorph in the solvent used. Because of the difference in free energy, the solubility of polymorphic forms differs from each other. SMT starts with dissolution of the metastable form followed by nucleation or growth of the more stable form. Most studies on SMT of small-molecule crystals report nucleation of the more stable form to be the rate-limiting step.82–84 Since secondary nucleation is frequently reported to dominate SMT, i.e., nucleation of a more stable polymorph on a less stable polymorph (often referred to as cross nucleation), the transition kinetics depend not only on the temperature and supersaturation but also on the number and CSD (i.e., the total crystal surface) of both phases.

Because of the supersaturation-dependence of the dissolution rates, growth rates, and nucleation rates (including secondary nucleation), temperature cycling can be utilized to control SMT.85–87 As such, the tubular crystallizer described in this work provides a powerful tool for speeding up a polymorphic transition under highly controlled process conditions. The continuous process benefits from a number of advantages discussed above.

In this study, we use the described tubular crystallizer to study SMT. D-Mannitol was chosen as model substance since the crystal structures of the polymorphs are known88 and their difference in free energy and solubility has extensively been reported.89,90 Because SMT proceeds via nucleation rather large temperature differences were chosen to promote nucleation events which was avoided for the fine removal and shape tuning studies.

5.1. Set-Up: Polymorphism Control of D-Mannitol.

Among the three polymorphs of D-mannitol, the most stable under environmental conditions and water is the β-form, followed by the α-form. The least stable is the δ-form. The α-form has little energetic difference from the β-form and similar physicochemical properties.91,92 The δ-form was shown to be kinetically stable during milling and after 5 years of storage at 25 °C and dry conditions. In pharmaceutical products, the β-form prevails since it is thermodynamically stable at RT, although the δ-form is increasingly used due to its superior compaction properties, e.g., for tableting93 and roller compaction.94

The (absolute) difference in free energy between these three polymorphs diminishes at lower temperatures and in ethanol–water mixtures, i.e., difference in solubility decreases with higher ethanol fractions. Therefore, a 60% ethanol and 40% water solution (w/w) solution was used for all polymorphism control experiments, preserving the stability of the α-polymorph (solid mass fractions, as described below) in the initial suspension for several hours, as shown in Figure S4. Solubility data for β-form in the used solvent mixture were determined as described in the Supporting Information, section S5.

The experimental procedure for the polymorphism studies of D-mannitol using a tubular crystallizer is shown in Figure 4, path C. Similar to the experiments shown in section 3 the solvent was saturated with D-mannitol (β-form) at 22 °C. Defined powder mixtures of two polymorphs (α-form: noncommercial, spray-dried type; β-form: Pearlitol 160C, both from Roquette, France) were added to the saturated solution (saturated with β-form of D-mannitol at 22 °C) to a solid mass fraction of 0.8% (w/w). Hence, the total amount of processed crystalline material was >5 g/h, which is enough for microscopic studies. However, industrial applications would require higher solid mass production rates. In order to minimize any size effects, sieved fractions of δ-mannitol (80–120 μm) were used in all polymorphism-control experiments. Rapid temperature cycling was performed by pumping the suspension through the tubing (same flow rates and length as used in the previous studies) immersed in water baths, cooled up to 10 °C and heated up to 40 °C. Because of the flow rates and the tube lengths the temperature in the suspension did not reach the respective temperature of the water baths. Using the model described in the Supporting Information (section S3), the minimum and maximum temperatures were estimated as T min = 11.6 °C and T max = 30.9 °C at the biggest temperature difference (see Figure S14), corresponding to super- and under saturations of S max = 1.90 and S min = 0.71.

Product samples were obtained by immediately filtering the product suspension while rinsing it with acetone in order to avoid that residual water induces additional polymorphic
transitions after the filtration. The polymorphic composition of the samples was determined via Raman spectroscopy (PerkinElmer Raman Station 400, Waltham, USA) and multivariate data analysis, i.e., by applying a PLS model. Details of the procedure, including processing of spectral data, generation and analysis of calibration sample, as well as a thorough description of the PLS model and its evaluation, are presented in the Supporting Information (section S4).  

5.2. Results and Discussion: Polymorphism Control of d-Mannitol. The mixtures of the α- and β-forms in the starting suspension and the composition of the product suspension after temperature cycling are listed in Table 2. For both powder mixtures, the fraction of the β-form in the product suspension increased and the α-form decreased. The higher the temperature difference of the water bath was, the more pronounced this was effect. The formation of the δ-form was never observed. Higher supersaturation is associated with higher nucleation rates, which agrees with an increase in the fraction of the β-form, associated with an increase in the temperature difference.

Primary nucleation was marginal as evident from preliminary studies cycling crystal-free solutions while monitoring the outlet with the high-speed camera and the micrographs of collected samples. As can be seen in Figure 8 and from quantification, the product crystals clearly show secondary nucleation of the β-form on the surface of the α-form crystals, indicating cross-nucleation. A comparison of micrographs shows a subsequent growth resulting in sea-urchin-like particles for all initial compositions and all temperature differences, but no significant number of fines. Although, the quantity of the β-form in the second starting suspension (50% w/w) was higher than in the first one (20% w/w), a similar or even higher amount of the β-form was generated during cycling, especially for the highest temperature difference. This indicates that SMT is governed by cross nucleation rather than by the growth of the seeded β-form crystals. For d-mannitol, it has been reported that an α-form seed crystal always induces the crystallization of the α-form and the β-polymorph seed yields the β- or α-form, whereas the δ-form seed yields the α-form.95 However, the β-form can nucleate on the α-form at high supersaturations, e.g., during quench-cooling.78 This agrees with our results showing cross nucleation of the β-form as was confirmed via Raman microscope studies on single particles as shown in Figure 9.

The tubular crystallizer can significantly accelerate SMT via temperature cycling as the difference in temperature increases, which is assigned to excessive secondary nucleation. Primary nucleation was prevented by keeping the time at supersaturation below the induction time. More cycles at high (or even higher) temperature differences seem to be the most convenient way to achieve a complete conversion to the β-form. This and the absence of moving parts with associated attrition facilitated the acceleration of SMT yielding big particles that can be filtered easily.

6. SUMMARY AND CONCLUSIONS

In this work a flexible tubular crystallizer operated in (gas–liquid) segmented-flow mode was developed. Four different objectives of advanced particle-engineering were successfully demonstrated, i.e., dispersed particle transport, fines removal, shape tuning, and polymorphic composition. Despite the simple setup, crystal engineering could be performed via a continuous process with a considerable volume (~liters per hour) and residence times in the order of several minutes. Precise control of the supersaturation is key for rational crystallization. By utilizing the heat transfer rates achievable in tubular crystallizer’s precise supersaturation levels could be obtained. Moreover, high levels of super- and undersaturation, and the ability to switch between them within seconds allows for rapid dissolution and growth, while preventing primary nucleation, as well as secondary nucleation if needed. This

| Table 2. Experimental Data Polymorphism Control |
|-----------------------------------------------|
| mass fractions in the start. susp. (as prepared) | temp. water bath 1 | temp. water bath 2 | mass fraction in the prod. susp. from Raman spectra and PLS model |
| (°C) | (°C) | α-form (%) | β-form (%) | α-form (%) | β-form (%) |
| starting susp. t = 0 min | 80 | 20 | 82 ± 4 | 18 ± 4 |
| starting susp. t = 60 min | 80 | 20 | 77 ± 4 | 23 ± 4 |
| ΔT = 30 °C | 80 | 20 | 10 | 40 | 59 ± 4 | 41 ± 4 |
| ΔT = 20 °C | 80 | 20 | 15 | 35 | 66 ± 4 | 34 ± 4 |
| ΔT = 10 °C | 80 | 20 | 20 | 30 | 68 ± 4 | 32 ± 4 |
| starting susp. t = 0 min | 50 | 50 | | | 53 ± 4 | 47 ± 4 |
| starting susp. t = 60 min | 50 | 50 | 10 | 40 | 56 ± 4 | 44 ± 4 |
| ΔT = 30 °C | 50 | 50 | 15 | 35 | 39 ± 4 | 61 ± 4 |
| ΔT = 20 °C | 50 | 50 | 20 | 30 | 49 ± 4 | 51 ± 4 |

Figure 8. (a) Microscope picture of spray-dried α-D-mannitol as received. (b) β-D-mannitol (Pearlitol 160C, Roquette, as received). Product crystals after temperature cycling (starting suspension: 80% α-form, 20% β-form) (c) ΔT = 20 °C, (d) ΔT = 30 °C.
occurs in the absence of any moving parts and at minimum agitation, while segmented flow allows for narrow residence time distributions.

However, achieving ideal plug flow characteristics for the particulate phase is not trivial as described above. Crystals can travel between slugs, if they become trapped in the wall film. Therefore, the wall film thickness should be smaller than the diameters of processed particulate matter. As shown in this section, the film thickness can be efficiently minimized by reducing the flow rates (which impairs particle dispersion in the segments), or using solvents with a higher surface tension (which is not always possible). Hence, the desired plug flow characteristics for liquid and solid phases in tubular reactors operated in segmented-flow mode can only be achieved at the right process settings in consideration of throughput and particle dispersion.

Fines removal via tubular crystallizers using segmented flow was studied via online laser diffraction, showing the potential of fast temperature cycling to shift the crystal size distribution significantly toward larger crystals within minutes. For the studied model system (D-mannitol, β-form) fines could be removed efficiently by increasing the temperature differences for cycling experiments. Other control options would be the number of cycles or the quantity of fed particles.

With respect to crystal shape tuning we showed how fast temperature cycling can be used to tune the shape of crystals. The studies using acetylsalicylic acid proved that facile control of the crystal shape is possible by manipulation of the number of cycles or the partitioning of heating and cooling segments. Other promising control options to tune crystal shapes in solution would be the temperature difference during cycling and changes in the solvent composition (not shown here).

The final section describes how fast changes in temperature, and hence switches between super- and undersaturation, affect solvent mediated phase transitions. For the tested transition, i.e., the transition from D-mannitol’s α-form to its β-form, cross nucleation of the β-form on the initially seeded α-form showed to be the rate-limiting step. Transitions became more efficient with increasing differences in temperature during cycling. Hence, the temperature difference during cycling can be used to control the transition kinetics. Since primary nucleation should be avoided (depending on the desired product crystal size distribution) this difference in temperature cannot be increased arbitrarily. Nevertheless, the number of cycles used provide a convenient design tool to further control the final polymorphic composition.

In summary, tubular crystallizers can be used to tune the physiochemical properties of crystalline matter in a short amount of time without using any additives.

**ASSOCIATED CONTENT**

Supporting Information
The Supporting Information (including the videos mentioned in the article) is available free of charge on the ACS Publications website at DOI: 10.1021/acs.cgd.7b01096.

Additional information about (1) used materials, (2) experimental procedures, and results, (3) the population balance and temperature models, and (4) the PLS model to quantify the α- and β-polymorph ratio via Raman spectroscopy (PDF)

Videos in AVI and MP3 format (ZIP)
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The authors declare no competing financial interest.

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