Uninformed Students: Student–Teacher Anomaly Detection with Discriminative Latent Embeddings

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Abstract—We introduce a simple, yet powerful student–teacher framework for the challenging problem of unsupervised anomaly detection and pixel-precise anomaly segmentation in high-resolution images. To circumvent the need for prior data labeling, student networks are trained to regress the output of a descriptive teacher network that was pretrained on a large dataset of patches from natural images. Anomalies are detected when the student networks fail to generalize outside the manifold of anomaly-free training data, i.e., when the output of the student networks differ from that of the teacher network. Additionally, the intrinsic uncertainty in the student networks can be used as a scoring function that indicates anomalies. We compare our method to a large number of existing deep-learning-based methods for unsupervised anomaly detection. Our experiments demonstrate improvements over state-of-the-art methods on a number of real-world datasets, including the recently introduced MVTec Anomaly Detection dataset that was specifically designed to benchmark anomaly segmentation algorithms.

1. Introduction

Unsupervised pixel-precise segmentation of regions that appear anomalous or novel to a machine learning model is an important and challenging task in many domains of computer vision. In automatic industrial inspection scenarios, it is often desirable to train models solely on a single class of anomaly-free images to segment defective regions during inference. In an active learning setting, regions that are detected as previously unknown by the current model can be included into the training set to improve the model’s performance.

Recently, efforts have been made to improve anomaly detection in one-class or multi-class classification scenarios [1, 2, 9, 10, 18, 25]. However, these algorithms assume that anomalies manifest themselves in the form of images of an entirely different class and a simple binary image-level decision whether the image is anomalous or not must be made. Little work has been directed towards the development of methods that can segment anomalous regions that only differ in a very subtle way from the training data manifold. Recently, Bergmann et al. [6] provided benchmarks for several state-of-the-art algorithms and identified a large room for improvement.

Existing works predominantly focus on generative algorithms such as Generative Adversarial Networks (GANs) [27, 28] or Variational Autoencoders (VAEs) [4, 32]. They detect anomalies using per-pixel reconstruction errors or by evaluating the density obtained from the model’s probability distribution. This has been shown to be problematic due to inaccurate reconstructions or poorly calibrated likelihoods [7, 19].

Discriminative embeddings from pretrained networks for transfer learning improve the performance of many supervised computer vision algorithms [15, 30]. For unsupervised anomaly detection, such approaches have not been thoroughly explored so far. Recent work suggests that these feature spaces generalize well for anomaly detection and even simple baselines outperform generative deep learning approaches [9, 22]. However, the performance of existing methods on large high-resolution image datasets is hampered by the use of shallow machine learning pipelines that require a dimensionality reduction of the used feature space. Moreover, they rely on heavy training data subsampling since their capacity does not suffice to model highly complex data distributions with a large number of training samples.

We propose to circumvent these limitations of shallow models by implicitly modeling the distribution of training features with a student–teacher approach. This leverages the high capacity of deep neural networks and frames anomaly detection as a feature regression problem. Given a descriptive feature extractor pretrained on a large dataset

Figure 1: Qualitative results of our anomaly detection method on the MVTec Anomaly Detection dataset. Top row: Defective input images. Center row: Ground truth regions of defects in red. Bottom row: Anomaly scores for each image pixel predicted by our algorithm.
Figure 2: Schematic overview of our approach. Input images are fed through a teacher network that densely extracts features for local image regions. An ensemble of \(M\) student networks is trained to regress the output of the teacher. During inference, the students will yield increased regression errors \(e\) and predictive uncertainties \(v\) in pixels for which the receptive field covers anomalous regions. Anomaly maps generated with different receptive fields can be combined for anomaly segmentation at multiple scales.

2. Related Work

There exists an abundance of literature on anomaly detection [24]. Deep-learning-based methods for the segmentation of anomalies strongly focus on generative models such as autoencoders [7] or GANs [27]. These attempt to learn representations from scratch, leveraging no prior knowledge about the nature of natural images, and segment anomalies by comparing the input image to a reconstruction in pixel space. This can result in poor anomaly detection performance due to simple per-pixel comparisons or imperfect reconstructions [7].

2.1. Anomaly Detection with Pretrained Networks

Promising results have been achieved by transferring discriminative embedding vectors of pretrained networks to the task of anomaly detection by fitting shallow machine learning models on the features of anomaly-free training data. Andrews et al. [2] use activations from different layers of a pretrained VGG network and model the anomaly-free training distribution with a \(\nu\)-SVM. However, they only apply their algorithm to image classification and do not consider the segmentation of anomalous regions. Similar experiments have been performed by Burlina et al. [9]. They report superior performance of discriminative embeddings compared to feature spaces obtained from generative models.

Nazare et al. [21] investigate the performance of different off-the-shelf feature extractors pretrained on an image classification task for the segmentation of anomalies in surveillance videos. Their approach trains a 1-Nearest-Neighbor (1-NN) classifier on embedding vectors extracted from a large number of anomaly-free training patches. Prior to the training of the shallow classifier, the dimensionality of the network’s activations is reduced using Principal Component Analysis (PCA). To obtain a spatial anomaly map during inference, the classifier must be evaluated for a large number of overlapping patches, which quickly becomes a performance bottleneck and results in rather coarse anomaly maps. Similarly, Napoletano et al. [20] extract activations from a pretrained ResNet-18 for a large number of cropped training patches and model their distribution using K-Means clustering after prior dimensionality reduction with PCA. They also perform strided evaluation of test images during inference. Both approaches sample training patches from the input images and therefore do not make use of all possible training features. This is necessary since, in their frame-
work, feature extraction is computationally expensive due to the use of very deep networks that output only a single descriptor per patch. Furthermore, since shallow models are employed for learning the feature distribution of anomaly-free patches, the available training information must be strongly reduced.

To circumvent the need for cropping patches and to speed up feature extraction, Sabokrou et al. [26] extract descriptors from early feature maps of a pretrained AlexNet in a fully convolutional fashion and fit a unimodal Gaussian distribution to all available training vectors of anomaly-free images. Even though feature extraction is achieved more efficiently in their framework, pooling layers lead to a downsampling of the input image. This strongly decreases the resolution of the final anomaly map, especially when using descriptive features of deeper network layers with larger receptive fields. In addition, unimodal Gaussian distributions will fail to model the training feature distribution as soon as the problem complexity rises.

2.2. Open-Set Recognition with Uncertainty Estimates

Our work draws some inspiration from the recent success of open-set recognition in supervised settings such as image classification or semantic segmentation, where uncertainty estimates of deep neural networks have been exploited to detect out-of-distribution inputs using MC Dropout [13] or deep ensembles [17]. Seeboeck et al. [29] demonstrate that uncertainties from segmentation networks trained with MC Dropout can be used to detect anomalies in retinal OCT images. Beluch et al. [5] show that the variance of network ensembles trained on an image classification task serves as an effective acquisition function for active learning. Inputs that appear anomalous to the current model are added to the training set to quickly enhance its performance.

Such algorithms, however, demand prior labeling of images for a supervised task by domain experts, which is not always possible or desirable. In our work, we utilize feature vectors of pretrained networks as surrogate labels for the training of an ensemble of student networks. The predictive variance together with the regression error of the ensemble’s output mixture distribution can then be used as a scoring function to segment anomalous regions in test images.

Figure 3: Pretraining of the teacher network $\hat{T}$ to output descriptive embedding vectors for patch-sized inputs. The knowledge of a powerful but computationally inefficient network $P$ is distilled into $\hat{T}$ by decoding the latent vectors to match the descriptors of $P$. We also experiment with embeddings obtained using self-supervised metric learning techniques based on triplet learning. Information within each feature dimension is maximized by decorrelating the feature dimensions within a minibatch.

3. Student–Teacher Anomaly Detection

This section describes the core principles of our proposed method. Given a training dataset $D = \{I_1, I_2, \ldots, I_N\}$ of anomaly-free images, our goal is to create an ensemble of student networks $S_i$ that can later detect anomalies in test images $J$, i.e., that can assign a score to each pixel as of how much it deviates from the training data manifold. For this, the student models are trained against regression targets obtained from a descriptive teacher network $T$ pretrained on a large dataset of natural images. After the training, anomaly scores can be derived for each image pixel from the students’ regression error and predictive variance. Given an input image $I \in \mathbb{R}^{w \times h \times C}$ of width $w$, height $h$, and number of channels $C$, each student $S_i$ in the ensemble outputs a feature map $S_i(I) \in \mathbb{R}^{w \times h \times d}$. It contains descriptors $y_{(r,c)} \in \mathbb{R}^d$ of dimension $d$ for each input image pixel at row $r$ and column $c$. By design, we limit the students’ receptive field, such that $y_{(r,c)}$ describes a square local image region $p_{(r,c)}$ of $I$ centered at $(r,c)$ of side length $p$. The teacher $T$ has the same network architecture as the student networks. However, it remains constant and extracts descriptive embedding vectors for each pixel of the input image $I$ that serve as deterministic regression targets during student training.

3.1. Learning Local Patch Descriptors

We begin by describing how to efficiently construct a descriptive teacher network $T$ using metric learning and knowledge distillation techniques. In existing work for anomaly detection with pretrained networks, feature extractors only output single feature vectors for patch-sized inputs or spatially heavily downsampled feature maps [20, 26]. In contrast, our teacher network $T$ efficiently outputs descriptors for every possible square of side length $p$ within the input image. $T$ is obtained by
first training a network $\hat{T}$ to embed patch-sized images $p \in \mathbb{R}^{p \times p \times C}$ into a metric space of dimension $d$ using only convolution and max-pooling layers. Fast dense local feature extraction for an entire input image can then be achieved by a deterministic network transformation of $T$ to $T$ as described in [3]. This yields significant speedups compared to previously introduced methods that perform patch-based strided evaluations. To let $T$ output semantically strong descriptors, we investigate both self-supervised metric learning techniques as well as distilling knowledge from a descriptive but computationally inefficient pretrained network. A large number of training patches $p$ can be obtained by random crops from any image database, e.g., ImageNet [16].

**Knowledge Distillation.** Patch descriptors obtained from deep layers of CNNs trained on image classification tasks perform well for anomaly detection when modeling their distribution with shallow machine learning models [20, 21]. However, the architectures of such CNNs are usually highly complex and computationally inefficient for the extraction of local patch descriptors. Therefore, we attempt to distill the knowledge of a powerful pretrained network $P$ into $\hat{T}$ by matching the output of $P$ with a decoded version of the descriptor obtained from $T$:

$$L_k(T) = ||D(\hat{T}(p)) - P(p)||^2.$$  

$D$ denotes a fully connected network that decodes the $d$-dimensional output of $T$ to the output dimension of the pretrained network’s descriptor.

**Metric Learning.** If for some reason pretrained networks are unavailable, one can also learn local image descriptors in a fully self-supervised way [11]. Here, we investigate the performance of discriminative embeddings obtained using triplet learning. For every randomly cropped patch $p$, a triplet of patches $(p, p^+, p^-)$ is augmented. Positive patches $p^+$ are obtained by small random translations around $p$, changes in image luminance, and the addition of Gaussian noise. The negative patch $p^-$ is created by a random crop from a randomly chosen different image. In-triplet hard negative mining with anchor swap [33] is used as a loss function for learning an embedding sensitive to the $l_2$ metric

$$L_m(T) = \max\{0, \Delta + \delta^+ - \delta^-\},$$

where $\Delta > 0$ denotes the margin parameter and in-triplet distances $\delta^+$ and $\delta^-$ are defined as:

$$\delta^+ = ||\hat{T}(p) - \hat{T}(p^+)||^2,$$

$$\delta^- = \min\{||\hat{T}(p) - \hat{T}(p^-)||^2, ||\hat{T}(p^+) - \hat{T}(p^-)||^2\}.$$

**Descriptor Compactness.** As proposed by Vassileios et al. [31], we minimize the correlation between descriptors within one minibatch of inputs $p$ in order to increase the descriptors’ compactness and remove unnecessary redundancy:

$$L_c(T) = \sum_{i \neq j} c_{ij},$$

where $c_{ij}$ denotes the entries of the correlation matrix computed over all descriptors $T(p)$ in the current mini-batch.

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**Table 1:** One-class classification results on MNIST and CIFAR-10. For each method, the average area under the ROC curve is given, computed across each dataset category. For our algorithm, we evaluate teacher networks trained with different loss functions. ✓ corresponds to setting the respective loss weight to 1, otherwise it is set to 0.

| Method      | MNIST          | CIFAR-10       |
|-------------|----------------|----------------|
| OCGAN       | 0.9750         | 0.6366         |
| 1-NN        | 0.9753         | 0.8189         |
| KMeans      | 0.9453         | 0.7592         |
| OC-SVM      | 0.9463         | 0.7388         |
| c2-AE       | 0.9383         | 0.7898         |
| VAE         | 0.9535         | 0.7502         |
| Ours ✓ ✓ ✓ ✓ | **0.9935**     | **0.8196**     |
| Ours ✓ ✓ ✓ ✓ | 0.9926         | 0.8035         |
| Ours ✓ ✓ ✓ ✓ | 0.9935         | 0.7940         |
| Ours ✓ ✓ ✓ ✓ | 0.9917         | 0.8021         |
Scoring Functions for Anomaly Detection. Having trained each student to convergence, a mixture of Gaussians can be obtained at each image pixel by equally weighting the ensemble’s predictive distributions.

From it, measures of anomaly can be obtained in two ways: First, we propose to compute the regression error of the mixture’s mean \( \mu_{(r,c)} \) with respect to the teacher’s surrogate label:

\[
e_{(r,c)} = ||\mu_{(r,c)} - (y^T_{(r,c)} - \mu)\text{diag} (\sigma)^{-1}||^2_2
\]

The intuition behind this score is that the student networks will fail to regress the teacher’s output within anomalous regions during inference since the corresponding descriptors have not been observed during training. Note that \( e_{(r,c)} \) is non-constant even for \( M = 1 \), where only a single student is trained and anomaly scores can be efficiently obtained with only a single forward pass through the student and teacher network, respectively.

As a second measure of anomaly, we compute for each pixel the predictive uncertainty of the Gaussian mixture as defined by Kendall et al. [13], assuming that the student networks generalize similarly for anomaly-free regions and differently in regions that contain novel information unseen during training:

\[
v_{(r,c)} = \frac{1}{M} \sum_{i=1}^M ||\mu_{(r,c)}^{S_i} - (y^T_{(r,c)} - \mu)\text{diag} (\sigma)^{-1}||^2_2.
\]

To combine the two scores, the means \( e_\mu, v_\mu \) and standard deviations \( e_\sigma, v_\sigma \) of all \( e_{(r,c)} \) and \( v_{(r,c)} \), respectively, over a validation set of anomaly-free images is computed. Summation of the normalized scores then yields the final anomaly score:

\[
\tilde{e}_{(r,c)} + \tilde{v}_{(r,c)} = \frac{e_{(r,c)} - e_\mu}{e_\sigma} + \frac{v_{(r,c)} - v_\mu}{v_\sigma}.
\]

Figure 4 illustrates the basic principles of our anomaly detection method on the MNIST dataset, where images with label 0 were treated as the normal class and all other classes were treated as anomalous. Since the images of this dataset are very small, we extracted a single feature vector for each image using \( \hat{T} \) and trained an ensemble of \( M = 5 \) patch-sized students to regress the teacher’s output. This results in a single anomaly score for each input image. Feature descriptors were embedded into 2D using multidimensional scaling [8] to preserve their relative distances.

3.3. Multi-Scale Anomaly Segmentation

If an anomaly only covers a small part of the teacher’s receptive field of size \( p \), the extracted feature vector predominantly describes anomaly-free traits of the local image region. Consequently, the descriptor can be predicted well by the students and anomaly detection performance will decrease. One could tackle this problem by downsampling the input image. This would, however, lead to an undesirable loss in resolution of the output anomaly map.

Our framework allows us explicit control over the size of the students’ and teacher’s receptive field \( p \). Therefore, we can detect anomalies at various scales by training multiple student–teacher ensemble pairs with varying values of \( p \). At each scale, an anomaly map with the same size as the input image is computed. Given \( L \) student–teacher ensemble pairs with different receptive fields, the normalized anomaly scores \( \tilde{e}_{(r,c)}^{(l)} \) and \( \tilde{v}_{(r,c)}^{(l)} \) of each scale \( l \) can be combined by simple averaging:

\[
\frac{1}{L} \sum_{l=1}^L \tilde{e}_{(r,c)}^{(l)} + \frac{1}{L} \sum_{l=1}^L \tilde{v}_{(r,c)}^{(l)}.
\]
distribution of pretrained networks. To do so, we compare to a K-Means classifier, a One-Class SVM (OCSVM), and a 1-NN classifier. They are fitted to the distribution of the teacher’s descriptors after prior dimensionality reduction using PCA. We also experiment with deterministic and variational autoencoders as deep distribution models over the teacher’s discriminative embedding. The $\ell_2$-reconstruction error [12] and reconstruction probability [1] are used as anomaly score, respectively. We further compare our method to recently introduced generative and discriminative deep-learning-based anomaly detection models and report improved performance over the state of the art. We want to stress that the teacher has not observed images of the evaluated datasets during pretraining to avoid an unfair bias.

As a first experiment and ablation study to find suitable hyperparameters, our algorithm is applied to a one-class classification setting on the MNIST and CIFAR-10 datasets. We then evaluate on the much more challenging MVTec Anomaly Detection (MVTec AD) dataset, which was specifically designed to benchmark algorithms for the segmentation of anomalous regions. It provides over 5000 high-resolution images divided into ten object and five texture categories. To highlight the benefit of our multiscale approach, an additional ablation study is performed on MVTec AD which investigates the impact of different receptive fields on the anomaly detection performance.

For our experiments, we use identical network architectures for the student and teacher networks, with receptive field sizes $p \in \{17, 33, 65\}$. All architectures are simple CNNs with only convolutional and max-pooling layers, using leaky rectified linear units (LReLU’s) with slope 0.005 as the activation function. Table 4 shows the specific architecture used for $p = 65$. For $p = 17$ and $p = 33$, similar architectures are given in Appendix A.

For the pretraining of the teacher networks $T$, triplets augmented from the ImageNet dataset are used. Images are zoomed to equal width and height sampled from $\{4p, 4p + 1, \ldots, 16p\}$ and a patch of side length $p$ is cropped at a random location. A positive patch $p^+$ for each triplet is then constructed by randomly translating the crop location within the interval $\{-\frac{p^1}{4}, \ldots, \frac{p^1}{4}\}$. Gaussian noise with standard deviation 0.1 is added to $p^+$. All images within a triplet are randomly converted to grayscale with a probability of 0.1. For knowledge distillation, we extract 512-dimensional feature vectors from the fully connected layer of a ResNet-18 that was pretrained for classification on the ImageNet dataset. For network optimization, we use the Adam optimizer [14] with an initial learning rate of $2 \times 10^{-4}$, a weight decay of $10^{-5}$, and a batch size of 64. Each teacher network outputs descriptors of dimension $d = 128$ and is trained for 50 000 iterations.

4.1. MNIST and CIFAR-10

Before considering the problem of anomaly segmentation, we evaluate our method on the MNIST and CIFAR-10 datasets, adapted for one-class classification. Five students are trained on only a single class of the dataset, while during inference images of the other classes must be detected as anomalous. Each image is zoomed to the students’ and teacher’s input size $p$ and a single feature vector is extracted for each image by passing it through the patch-sized networks $T$ and $\hat{T}$. We experiment with differently pretrained teacher networks, varying the weights $\lambda_k, \lambda_m, \lambda_c$ in the teacher’s loss function $L(T)$. The patch size for the experiments in this subsection is set to $p = 33$. As a measure of anomaly detection performance, the area under the ROC curve (AUC) is evaluated. Shallow and deep distributions models are trained on the teacher’s descriptors of all available in-distribution samples. We additionally report numbers for OCGAN [23], a recently proposed generative model directly trained on the input images. Detailed information regarding training parameters for all methods on this dataset can be found in Appendix B.

Table 1 shows our results. Our approach outperforms the other methods for a variety of hyperparameter settings. Distilling the knowledge of the pretrained ResNet-18 into the teacher’s descriptor yields slightly better performance than training the teacher in a fully self-supervised way using triplet learning. Reducing descriptor redundancy by minimizing the correlation matrix yields improved results. On average, shallow models and autoencoders fitted to our teacher’s feature distribution outperform OCGAN but do not reach the performance of our approach. Since for 1-NN, every single training vector can be stored, it performs exceptionally well on these relatively small datasets. On
Table 3: Performance of our algorithm on the MVTec AD dataset for different receptive field sizes $p$. Combining anomaly scores across multiple receptive fields shows increased performance for many of the dataset’s categories. We report the normalized area under the PRO-curve up to an average false positive rate per-pixel of 30%.

Table 4: General outline of our network architecture for training teachers $\hat{T}$ with receptive field size $p = 65$. Leaky rectified linear units with slope 0.005 are applied as activation functions after each convolution layer. Architectures for $p = 17$ and $p = 33$ are given in Appendix A.

is computed. We evaluate the PRO value for a large number of increasing thresholds until an average per-pixel false positive rate of 30% for the entire dataset is reached and integrate the area under the PRO curve as a measure of anomaly detection performance. Note that for high false positive rates, large parts of the input images would be wrongly labeled as anomalous and even perfect PRO values of 1.0 would no longer be meaningful. We normalize the integrated area to a maximum achievable value of 1.0.

Table 2 shows our results training each algorithm with a receptive field of $p = 65$ for comparability. Our method consistently outperforms all other evaluated algorithms for almost every dataset category. The shallow machine learning algorithms fitted directly to the teacher’s descriptors after applying PCA do not manage to perform satisfactorily for most of the dataset categories. This shows that their capacity does not suffice to accurately model the large number of available training samples. The same can be observed for the CNN-Feature Dictionary. As it was the case in our previous experiment on MNIST and CIFAR-10 experiments. Ensembles were trained with $M = 3$ students.

For training shallow classifiers on the teacher’s output descriptors, a subset of vectors is randomly sampled from the teacher’s feature maps. Their dimension is then reduced by PCA, retaining 95% of the variance. The variational and deterministic autoencoders are implemented using a simple fully connected architecture and are trained on all available descriptors. In addition to the models directly fitted to the teacher’s feature distribution, we benchmark our approach against the best performing deep learning based methods presented by Bergmann et al. [6] on this dataset. Specifically, these methods include the CNN-Feature Dictionary [20], the SSIM-Autoencoder [7], and AnoGAN [27]. Hyperparameters for each evaluated method are detailed in Appendix C.

We compute a threshold-independent measure based on the per-region-overlap (PRO) as the evaluation metric. It weights ground-truth regions of different size equally, which is in contrast to simple per-pixel measures for which a single large correctly segmented region can make up for many incorrectly segmented small ones. It was also used by Bergmann et al. in [6]. For computing the PRO metric, anomaly maps are first thresholded at a given anomaly score to make a binary decision for each pixel whether an anomaly is present or not. For each connected component within the ground-truth, the percentage of overlap with the thresholded anomaly region is computed. We evaluate the PRO value for a large number of increasing thresholds until an average per-pixel false positive rate of 30% for the entire dataset is reached and integrate the area under the PRO curve as a measure of anomaly detection performance. Note that for high false positive rates, large parts of the input images would be wrongly labeled as anomalous and even perfect PRO values of 1.0 would no longer be meaningful. We normalize the integrated area to a maximum achievable value of 1.0.

Table 3 shows the performance of our algorithm for different receptive field sizes $p \in \{17, 33, 65\}$ and when combining multiple scales. For some objects, such as bottle and cable, larger receptive fields yield better results. For others, such as wood and toothbrush, the inverse behavior can be observed. Combining multiple scales enhances the performance for many of the dataset categories. A qualitative example highlighting the benefit of our multi-scale anomaly segmentation is visualized in Figure 5.
5. Conclusion

We have proposed a novel framework for the challenging problem of unsupervised anomaly segmentation in natural images. Anomaly scores are derived from the predictive variance and regression error of an ensemble of student networks, trained against surrogate labels obtained from a descriptive teacher network. Ensemble training can be performed end-to-end and purely on anomaly-free training data without requiring prior data annotation. Our approach can be easily extended to detect anomalies at multiple scales. We demonstrate improvements over current state-of-the-art methods on a number of real-world computer vision datasets for one-class-classification and anomaly segmentation.

Appendix A.
Network Architectures

A description of the network architecture for a patch-sized teacher network \( \hat{T} \) with receptive field of size \( p = 65 \) can be found in our main paper. Architectures for teachers with receptive field sizes \( p = 33 \) and \( p = 17 \) can be found in Tables 5a and 5b, respectively. Leaky rectified linear units with slope 0.005 are used as activation function after each fully connected layer.

Appendix B.
Experiments on MNIST and CIFAR-10

We give details about additional hyperparameters for our experiments on the MNIST and CIFAR-10 datasets. We additionally provide the per-class ROC-AUC values for the two datasets in Tables 6 and 7, respectively.

Hyperparameter Settings. For the deterministic \( \ell_2 \)-autoencoder (\( \ell_2 \)-AE) and the variational autoencoder (VAE), we use a fully connected encoder architecture of shape 128–64–32–10 with leaky rectified linear units of slope 0.005. The decoder is constructed in a manner symmetric to the encoder. Both autoencoders are trained for 100 epochs at an initial learning rate of 0.01 using the Adam optimizer and a batch size of 64. A weight decay of rate \( 10^{-5} \) is applied for regularization. To evaluate the reconstruction probability of the VAE, five independent forward passes are performed for each feature vector. For the OCSVM, the radial basis function kernel is used. K-Means is trained with ten cluster centers and the distance to the nearest cluster center in the feature space during inference. The OCSVM is evaluated with a radial basis function as the kernel.

Deep-Learning Based Models. For evaluation on MVTec AD, the architecture of the \( \ell_2 \)-AE and VAE are identical to the ones used on the MNIST and CIFAR-10 dataset. Each fully connected autoencoder is trained for 100 epochs, at an initial learning rate of \( 10^{-4} \) and weight decay of \( 10^{-5} \). Batches are constructed from 512 randomly sampled vectors of the teacher’s feature maps. The reconstruction probability of the VAE is computed by five individual forward passes through the network. For the evaluation of AnoGAN, the SSIM-Autoencoder, and the CNN-Feature Dictionary, we use the same hyperparameters as Bergmann et al. in the MVTec AD dataset paper [6]. Only a slight adaption is applied to the CNN-Feature Dictionary by cropping patches of size \( p = 65 \) and performing the evaluation by computing anomaly scores for overlapping patches with a stride of four pixels.

Appendix C.
Experiments on MVTec AD

We give additional information on the hyperparameters used in our experiments on MVTec AD for both shallow machine learning models as well as deep learning methods.

Shallow Machine Learning Models. For the 1-NN classifier, we construct a dictionary of 5000 feature vectors and take the distance to the closest training sample as the anomaly score. For the other shallow classifiers, we fit their parameters on 50,000 training samples, randomly chosen from the teacher’s feature maps. The K-Means algorithm is run with ten cluster centers and measures the distance to the nearest cluster center in the feature space during inference. For 1-NN, the feature vectors of all available training samples are stored and tested during inference.

Deep-Learning Based Models. For evaluation on MVTec AD, the architecture of the \( \ell_2 \)-AE and VAE are identical to the ones used on the MNIST and CIFAR-10 dataset. Each fully connected autoencoder is trained for 100 epochs, at an initial learning rate of \( 10^{-4} \) and weight decay of \( 10^{-5} \). Batches are constructed from 512 randomly sampled vectors of the teacher’s feature maps. The reconstruction probability of the VAE is computed by five individual forward passes through the network. For the evaluation of AnoGAN, the SSIM-Autoencoder, and the CNN-Feature Dictionary, we use the same hyperparameters as Bergmann et al. in the MVTec AD dataset paper [6]. Only a slight adaption is applied to the CNN-Feature Dictionary by cropping patches of size \( p = 65 \) and performing the evaluation by computing anomaly scores for overlapping patches with a stride of four pixels.
Table 7: CIFAR-10 results.

| Method   | 0   | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | Mean  |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-------|
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.999 | 0.999 | 0.990 | 0.993 | 0.992 | 0.993 | 0.997 | 0.995 | 0.986 | 0.991 | 0.9935 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.999 | 0.999 | 0.997 | 0.999 | 0.995 | 0.994 | 0.995 | 0.993 | 0.992 | 0.9926 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.999 | 0.999 | 0.992 | 0.998 | 0.992 | 0.993 | 0.993 | 0.995 | 0.988 | 0.992 | 0.9935 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.999 | 0.999 | 0.989 | 0.990 | 0.990 | 0.997 | 0.993 | 0.981 | 0.989 | 0.9917 |

Table 6: MNIST results.

| Method   | 0   | 1   | 2   | 3   | 4   | 5   | 6   | 7   | 8   | 9   | Mean  |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-------|
| OCGAN    | 0.757 | 0.531 | 0.640 | 0.620 | 0.723 | 0.620 | 0.723 | 0.575 | 0.820 | 0.554 | 0.6566 |
| 1-NN     | 0.792 | 0.860 | 0.746 | 0.729 | 0.815 | 0.797 | 0.876 | 0.836 | 0.856 | 0.882 | 0.8189 |
| KMeans   | 0.673 | 0.822 | 0.665 | 0.676 | 0.742 | 0.746 | 0.828 | 0.780 | 0.817 | 0.843 | 0.7592 |
| OC-SVM   | 0.651 | 0.785 | 0.618 | 0.679 | 0.733 | 0.730 | 0.797 | 0.760 | 0.799 | 0.836 | 0.7388 |
| t2-Æ     | 0.747 | 0.862 | 0.690 | 0.698 | 0.788 | 0.739 | 0.849 | 0.824 | 0.812 | 0.869 | 0.7898 |
| VAE      | 0.705 | 0.819 | 0.605 | 0.700 | 0.734 | 0.731 | 0.797 | 0.751 | 0.801 | 0.839 | 0.7502 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.789 | 0.849 | 0.734 | 0.748 | 0.851 | 0.793 | 0.892 | 0.830 | 0.862 | 0.848 | 0.8196 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.784 | 0.836 | 0.706 | 0.742 | 0.826 | 0.768 | 0.870 | 0.815 | 0.857 | 0.831 | 0.8035 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.804 | 0.855 | 0.706 | 0.709 | 0.798 | 0.738 | 0.860 | 0.797 | 0.849 | 0.824 | 0.7940 |
| Ours     | ✓   | ✓   | ✓   | ✓   | 0.766 | 0.817 | 0.715 | 0.736 | 0.855 | 0.763 | 0.885 | 0.819 | 0.838 | 0.827 | 0.8021 |

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