A Single-Level Tunnel Model to Account for Electrical Transport through Single Molecule- and Self-Assembled Monolayer-based Junctions

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We present a theoretical analysis aimed at understanding electrical conduction in molecular tunnel junctions. We focus on discussing the validity of coherent versus incoherent theoretical formulations for single-level tunneling to explain experimental results obtained under a wide range of experimental conditions, including measurements in individual molecules connecting the leads of electromigrated single-electron transistors and junctions of self-assembled monolayers (SAM) of molecules sandwiched between two macroscopic contacts. We show that the restriction of transport through a single level in solid state junctions (no solvent) makes coherent and incoherent tunneling formalisms indistinguishable when only one level participates in transport. Similar to Marcus relaxation processes in wet electrochemistry, the thermal broadening of the Fermi distribution describing the electronic occupation energies in the electrodes accounts for the exponential dependence of the tunneling current on temperature. We demonstrate that a single-level tunnel model satisfactorily explains experimental results obtained in three different molecular junctions (both single-molecule and SAM-based) formed by ferrocene-based molecules. Among other things, we use the model to map the electrostatic potential profile in EGaIn-based SAM junctions in which the ferrocene unit is placed at different positions within the molecule, and we find that electrical screening gives rise to a strongly non-linear profile across the junction.

The last decade has led to substantial advances in the understanding of electrical conduction through molecular systems, mostly due to an improved control of the different measuring techniques employed to study molecular junctions, including electromigrated single-electron transistors (SETs)¹⁻⁸, scanning tunneling microscopy (STM) break-junctions⁹,¹⁰, and techniques enabling measuring self-assembled monolayers (SAMs) of molecules sandwiched between two macroscopic electrodes¹¹⁻²⁰. By far most fabrication techniques produce two-terminal junctions in the form of electrode-molecule-electrode, with either a single molecule or a self-assembled monolayer (SAM) as the active component. However, the lack of an electrical gating capability in two-terminal junctions complicates determination of the energy level alignment. STM break-junctions can be used to obtain statistics on electron transport at an individual molecular level but the supramolecular and the electronic structure of the junctions cannot be investigated independently. By contrast, it is possible to measure both the supramolecular and electronic structure of the SAMs immobilized on one of the electrodes (usually referred to as the bottom-electrode) using standard surface characterization techniques before fabrication of the top-contact. For most systems, however, it is not clear how much the energy level alignment changes once the molecules are in...
contact with the top-electrodes and therefore models are often used to extract the relevant transport parameters. From a technological point of view, SAM-based junctions are promising candidates for molecular electronics technologies, with rectification ratios rapidly approaching values of commercial semiconductor devices. On the other hand, three-terminal SETs electrically gate the molecular electronic states of an individual molecule, enabling the full spectroscopic resolution of the molecular energy landscape. Comparative studies using these different techniques are required to establish the principles governing electrical conduction through molecular tunnel junctions under a wide range of experimental conditions.

Despite the increasing number of experimental reports, and to a lesser extent theoretical works, dedicated to the topic of electrical conduction through molecular junctions (see refs 24–26 and references therein), there remains the challenge of extracting fundamental characteristic junction parameters from the experiments in a consistent way. The complexity of the real devices, with large variations in the parameters that affect electrical conduction, and the different possible transport regimes, make the rigorous treatment of electron transport through junctions extremely difficult. In this context, first-principles calculations have the advantage that one can account for structural details of the junctions. However, they are not generally applicable (i.e., they need to be tailored to the specific junction under study) and may require very long calculation times even on high-performance computing platforms. Alternatively, analytical models dealing mainly with the energetics of the junction, such as the Landauer formalism for coherent tunneling (or the rate equations for incoherent tunneling), are easy to employ but rely on rough approximations of some critical parameters and may miss some of the physics involved in the process, particularly when conduction is driven or assisted by interactions with the molecular surroundings (e.g., reorganization energies, many-body interactions, energy level renormalization, image charges, etc.).

There are ongoing theoretical efforts focused on solving the problem by integrating different effects to formulate a non-equilibrium model that includes the above mentioned hamiltonian in terms of molecular excitations. When computing electron transport through molecular junctions (for a detailed discussion on this see ref. 26). This is far from the present work, where we do not attempt to develop a new theory but instead aim to test the applicability of a well-known single-level tunneling model and variations thereof, to capture the essential physics of molecular junctions. The key metric for success of our model is the ability to easily implement it using experimentally obtained input parameters. In this article, we test this single-level tunneling model using properties of molecular diodes measured in two different test-beds: (i) Three-terminal SET experiments performed at different temperatures on individual S(CH₂)₈Fc(CΗ₂)₂S molecules; and (ii) experiments in SAM-based EGaIn junctions of S(CH₂)₃Fc₂ molecules where two distinct molecular levels participate in charge transport. In addition, we employ the model to interpret experiments performed on SAM-based EGaIn junctions of S(CH₂)₃FeC₃₃– molecules where the ferrocene (Fc) unit is placed at different positions (n) within the alkyl chain. Fitting our model to the experimental data enables the determination of the electrostatic potential profile in the junction, which we find to be strongly non-linear, indicating the presence of significant electrical screening in the junction. Comparison between the different junctions shows that the single-level tunneling model satisfactorily describes both single molecule and SAM based junctions. The model captures the essential physics, including the asymmetry of the I(V) curves, the shape of the electrostatic potential profile and the temperature dependence of the transport excitations. Finally, we use this model to discuss in detail the range of validity of coherent versus incoherent theoretical formulations that have been used to rationalise some recent experimental results.

Results

The single-level transport model: Coherent versus incoherent tunneling. In the simplest approximation, a molecular junction can be represented by the schematic diagrams shown in Fig. 1, where the molecule sandwiched between two electrodes (in a discrete set of levels (with N representing the number of electrons in each level)) separated from the electrostatic potential in the electrodes by tunnel barriers. The molecular levels closest to the electrostatic potentials of the leads at zero bias are known as the HOMO (highest occupied molecular orbital, N) and LUMO (lowest unoccupied molecular orbital, N + 1) levels and are well separated in energy by a ~2–5 eV conductance gap in solid state junctions. The level closest to the Fermi energy of the electrodes governs the electrical conduction through the junctions for moderate bias potentials.

Conduction through a molecule can, in principle, be understood in terms of sequential tunneling (either coherent or incoherent) involving one molecular level. In such a process the electron tunnels from the source into the molecule at a rate γᵣ and then out into the drain lead at a rate γᵣ. The ratio between these rates and the characteristic intramolecular relaxation times determines whether the electron transport occurs coherently or incoherently. This means that if the electron spends sufficient time inside the molecule to significantly couple with internal/external degrees of freedom (i.e., short relaxation time and short decoherence time relative to the tunneling rates) then the process will become incoherent, with an associated loss of phase in the case of elastic tunneling, and loss of both phase and energy in the case of inelastic tunneling. In wet electrochemical molecular charge-transfer processes, energy relaxation is usually facilitated by intramolecular vibrational modes and polaron excitations in the surrounding solvent molecules. In terms of Marcus theory, these are known as inner- and outer-sphere molecular reorganization processes, respectively, and are characterized by an activation energy arising from the classical energy barrier governing the process. At sufficiently high temperatures, these processes lead to an exponential increase of the charge transfer (accompanied by an Arrhenius law and incoherent tunneling). However, in the junctions discussed in this work, where the molecules are present in solid-state devices and charge transport is studied in the absence of solvent, outer-sphere reorganization processes do not likely play an important role in the electrical conduction through the junction. This is not necessarily the case in all SAM-based junctions, since even in the absence of solvent molecules, neighboring molecules can play this role, particularly when considering complex molecules with high degrees of polarizability.
We expect that inner-sphere reorganization will always be important, and can be related to intra-molecular vibrational modes with energies usually below a few tens of millielectronvolts ($\lesssim 30 \text{ meV}$), which is smaller than or comparable to other energy scales relevant to the conduction process, such as thermal broadening at high temperatures ($k_B T = 13–86 \text{ meV}$ in the range 100–1000 K). Thus, when only one level participates in the conduction through the junction (which may be the case in many molecular junctions), the vibrational modes can be formally incorporated into an effective temperature-dependent level broadening (the higher the temperature the more vibrational modes will be sampled), which means that it is reasonable to still treat the transport process with simple single-level transport models, as we do in the present work. Note the different causes of level broadening, which we can separate into two main contributions: (i) broadening due to the coupling of the molecule to the electrodes, with tunneling rate $\gamma = \gamma_L + \gamma_R$, and, (ii) broadening arising from the coupling of the electron to other degrees of freedom of the molecule, $\gamma_0$. Of course, this is just a simplification (virtual transitions to high-energy molecular states take place during the conduction process, leading to renormalized parameters) and should be taken as such. However, this picture can be justified from a more fundamental calculation involving a non-equilibrium quantum mechanical treatment of the response of the molecule to its coupling to leads. When a single energy level is active in the molecule, and the coherent interactions between electrons in the molecule and those in the leads are negligible, the non-equilibrium expression for the current reduces to an expression similar to the Landauer-Büttiker formula

$$I = \frac{2e^2}{h} \int dE \left[ f \left( \frac{E - \mu_L}{k_B T} \right) - f \left( \frac{E - \mu_R}{k_B T} \right) \right] \text{Tr} \left[ \frac{\gamma_L(E)\gamma_R(E)}{\gamma_L(E) + \gamma_R(E)} \text{Im}[G'(E)] \right],$$

(1)

where $f(x) = 1/(e^{x} + 1)$, $\mu_L$ and $\mu_R$ are the chemical potential at the leads, $\gamma_L(E)$ and $\gamma_R(E)$ are the partial level widths due to the coupling to right and left leads, respectively, and $G'$ is the molecule's single-particle retarded Green's function, which contains a self-energy that takes into account the coupling to leads and to other degrees of freedom as an imaginary part, namely, a total level width. In fact, this has been the starting point of several successful theoretical descriptions of molecular electronic transport experiments (see, e.g., refs 35,36).

We acknowledge that there may be other processes playing important roles in the transport through solid-state junctions, such as intermolecular interactions or electrostatic potential changes due to electron charging or image-charge effects, among others. Some of these could be incorporated into simple single-level transport models. As we show below, for a single-level junction system the coherent and incoherent tunneling treatments provide identical predictions of the current at all temperatures, provided that one incorporates into the level broadening the two effects discussed above concerning outer-sphere reorganization and vibrational modes. Therefore, even a single-level coherent transport model can explain the exponential thermal enhancement of the conductance through a molecular junction without the need to invoke Marcus relaxation processes.
This is because the temperature dependence of the conductance naturally arises from the thermal broadening of the energy of the electrons in the leads (see, e.g., the work by van der Zant et al.37). In other words, a transition between a plateau-like to temperature-dependent conductance in a molecular junction should not be taken as conclusive proof of inelastic incoherent tunneling. Sequential tunneling may well be coherent and one simply cannot distinguish them when transport involves a single energy level without considering the ratio of the relaxation rates involved.

As mentioned before, the transition between coherent and incoherent tunneling is determined by the tunneling rates in and out of the molecule (when compared with the intrinsic molecular relaxation rates). As explained by Moth-Poulsen and Bjørnholm in their review article38, the tunneling rates for a complex molecule usually depend on the strength of the bond of the molecule to the electrodes, $E_{b0}$, and on the intramolecular coupling, $t_i$, between the electrode and the molecular frontier orbital (see Fig. 1a), and are, in general, difficult to engineer. As mentioned above, the molecule-electrode couplings result in broadening of the molecular levels ($\gamma = \gamma_L + \gamma_R$). The capacitive couplings of the frontier orbital with the electrodes determine the electric potential drops at both sides of the active conduction unit ($V_L$ and $V_R$) and provide asymmetry to the junctions when $L = L_R$. This asymmetry is parameterized by the dimensionless division parameter $\eta = V_L/(V_L + V_R)$, which gives the ratio of the voltage drop between the molecule and the right electrode with respect to the total voltage drop in the junction.

The molecular frontier orbital follows the average effective potential within the molecule and its energy can be expressed as $E_m = \mu_k(V) + \varepsilon + \eta q V$, where $\varepsilon$ is the zero-bias energy offset between the molecular orbital and the electrodes, $q$ is the electron charge, and $\mu_k$ is the electrochemical potential of the right electrode. The behaviour of $E_m$ with respect to the bias potential $V$ is shown in Fig. 2 for different values of $\eta$. For $\eta = 0$, the zero-bias energy of the level remains constant as the bias potential is increased, while for $\eta = 0$ or $\eta = 1$, the molecular level closely follows the right or left potentials, respectively.

Finally, thermal broadening of the energy of the electrons in the leads also greatly affects conduction through the junction and needs to be taken into account. When a bias potential is applied, two distinct Fermi distributions need to be used, one for each lead:

$$f_{L,R}(E) = \frac{1}{1 + \exp[(E - \mu_{L,R})/k_B T]}$$

In the case of a single conduction level, the electrical current can be calculated by solving the rate equations for each side of the molecule (see Supplemental Information for a generalized treatment of the rate equations for a molecule with multiple levels). In the limit of very small broadening ($\gamma \ll k_B T$, $|\varepsilon| \ll |\mu_L - \mu_R|$), one obtains the following electrical current expression (see detailed discussion in Supplemental Information and in refs 24,39):

$$I_{L,R}(E) = (-q) \frac{\gamma_{L,R}}{h} (f_{L,R}(E) - N),$$

where $N$ is the occupation number or average number of electrons in the steady state. By definition, in this state there is no net transfer of electrons in or out of the junction (i.e., $I_L + I_R = 0$), from which one can extract an expression for $N$:

$$N = \frac{\gamma_L f_L(E) + \gamma_R f_R(E)}{\gamma_L + \gamma_R}$$
Substituting this functional for \( N \) in Eq. (3) one obtains the steady-state current through the junction (without taking into account the spin) as

\[
I = I_L = - I_R = \frac{2q}{\hbar} \gamma_{L} \gamma_{R} \left[ f_L(E) - f_R(E) \right].
\]

Note that this treatment accounts for sequential tunneling of the electron from one of the leads into the molecule and further into the opposite lead and is incoherent in nature. In other words, the rate equations formulation assumes that the electron’s phase memory is completely lost once it tunnels into the molecule. That can only happen through relaxation processes—purely elastic in the case of a single level (no other levels to transit into), but possibly even inelastic. Apart from this, the first conclusion that one can extract from this simple expression is that current will only flow through the junction if a molecular level lies between the electrochemical potentials of the left and right electrodes (i.e., within the conductance window). Of course, this approximation fails when the level width surpasses such energy separation, since it will lie partially out of the conductance window. In other words, the current will not increase indefinitely by simply increasing the level width (i.e., increasing the coupling to the electrodes). On the other hand, the resistance has a quantum mechanical limit, which for a single transport channel translates into a universal quantum of conductance, \( G_0 \), as originally predicted by Landauer.

Interestingly, it is possible to relax the condition of very small broadening \( \gamma \ll k_B T, \varepsilon \), \( |\mu_L - \mu_R| \) and incorporate the effect of a finite level broadening into the rate equation calculation by introducing a broadened density of states (DOS) in the shape of a Lorentzian centered at the energy level \( \varepsilon \),

\[
D_{\varepsilon}(E) = \frac{\gamma/2\pi}{(E - \varepsilon)^2 + (\gamma/2)^2}. \tag{6}
\]

The result is

\[
I = \frac{q}{\hbar} \int_{-\infty}^{\infty} dE \ D_{\varepsilon}(E) \frac{-\gamma_{L} \gamma_{R}}{\gamma_{L} + \gamma_{R}} \left[ f_L(E) - f_R(E) \right]. \tag{7}
\]

This expression matches exactly the one derived by Jauho, Wingreen, and Meir in 1994 using a fully coherent formulation based on the Keldysh Green’s function formalism (see Supplemental Information for a detailed discussion of this point). This may seem remarkable, but we note that for a single channel and a single level in the molecule, interference plays no role in the electron conduction through the molecule. As a result, coherent and incoherent sequential tunneling cannot be distinguished at a formal level. Both models provide the same level of accuracy in describing transport at low bias through a single level, as was verified in a pioneering experiment by the Saclay group.

In the standard derivation of Eq. (7) in the context of coherent tunneling, the level broadening is entirely given by the sum of the partial broadenings due to leakage through the leads (\( \gamma = \gamma_L + \gamma_R \)). In the derivation based on rate equations (incoherent sequential tunneling) one can introduce an additional source of broadening unrelated to leakage, namely, \( \gamma = \gamma_L + \gamma_R + \gamma_0 \). Other than that, the two results are formally identical at any temperature or bias voltage.

Landauer derived an equation similar to Eq. (7) under the assumption that the entire system (leads and “molecule”) were one dimensional. But now we know that the validity of Eq. (7) does not depend on the spatial dimensions, but rather on the number of channels involved. Namely, it is a correct description only in the case of a single channel in and out of the molecule on each lead. The derivation presented here is also only valid in the case of spinless charge carriers. It is straightforward to extend it to include spin \( \frac{1}{2} \) carriers; provided that coherence does not extend beyond the molecule, both rate equation and fully-coherent formulations yield again identical results. When the charging energy is strong and forbids double occupancy of the molecular level (that is, \( E_c \gg k_B T \), \( |\mu_L - \mu_R| \) which is typically the case for solid-state molecular junctions), the expression for the current becomes

\[
I = \frac{2q}{\hbar} \int_{-\infty}^{\infty} dE \ D_{\varepsilon}(E) \frac{-\gamma_{L} \gamma_{R}}{\gamma_{L} + \gamma_{R} + \Gamma_{0 \rightarrow 1}} \left[ f_L(E) - f_R(E) \right], \tag{8}
\]

where the level width associated to the level lifetime is given by

\[
\Gamma_{0 \rightarrow 1} = \int_{-\infty}^{\infty} dE \ D_{\varepsilon}(E) \left[ \gamma_L f_L(E) + \gamma_R f_R(E) \right]. \tag{9}
\]

In the linear regime and when the molecular level falls within the bias voltage window, \( \Gamma_{0 \rightarrow 1} \approx \gamma_R + \gamma_L \) and one finds that the current matches closely that of Eq. (7), with the prefactor of 2 cancelling out. Notice that, in the opposite limit, when charging energy is weak and double occupancy is permitted, one can simply adopt Eq. (7) and account for spin degeneracy in the conduction process by multiplying the right-hand side by a factor of 2 (see Supplemental Information for details).

Thus, it is our claim that Eq. (7) can be formally taken as a good approximation to describe conduction through a molecular junction at all temperatures provided that: (i) Electrical conduction through the junction is mainly governed by a single level (no transitions to high-energy states); and, (ii) that intra- and inter-molecular interactions can be incorporated into the level width (elastic processes). These conditions are likely to be applicable to solid-state molecular junctions, where interaction with solvent molecules is not possible and Marcus-like energy relaxation processes are unlikely.
It is easy to see from Eq. (7) that at low temperature ($T = 1$ if $\mu_L < E < \mu_R = 0$ otherwise) and low bias ($\mu_L \approx \mu_R$), the maximum conductance (occurring when the energy level coincides with the average electrochemical potential, $\bar{\epsilon} = \mu$) will be

$$G_{\text{max}} = \frac{I}{V} = \frac{q^2}{\hbar} \frac{4\gamma_L\gamma_R}{(\gamma_L + \gamma_R)^2}.$$  

(10)

this expression coincides with the universal conductance $G_0 = \frac{q^2}{\hbar}$, if the two rates are equal ($\gamma_L = \gamma_R$) [for the spinless case].

As a side note, one can break up the Landauer conductance into two contributions, since

$$G^{-1} = \frac{\hbar^2 I}{q^2 M T} = \frac{\hbar^2 I}{q^2 M} + \frac{\hbar^2 I - T}{q^2 M} = G_C^{-1} + G_T^{-1},$$

(11)

with $M$ representing the number of channels and the characteristics of the junction (see Eq. (8) when $\gamma_L \approx \gamma_R$). This is convenient in order to separate the contact resistance ($G_C^{-1}$) from the tunneling resistance ($G_T^{-1}$) in a molecular junction, and particularly relevant for AC impedance transport measurements, where one can distinguish experimentally between capacitive and resistive contributions in the transport through the junction.$^{13}$

Figure 3. **Coherent vs. Incoherent tunnelling.** The electrical current through a single-level molecular junction as expressed by Eqs (7) (broadened molecular level) and (5) (zero-width molecular level). The parameters used in the calculations are $\epsilon = 0.4$ eV, $\eta = 0.5$, $V_g = 0$, and $\gamma_L = \gamma_R = 1$ meV for (a–c) and $\gamma_L = \gamma_R = 10$ meV for (d), which are typical values in the molecular junctions studied in this work. The plateau at low temperatures is a direct consequence of the broadening of the molecular level as given by Eq. (6), which sets a maximum for a conductance at low temperatures.
An interesting exercise within the context of the discussion in this article is to solve the asymptotic limit of Eq. (7) at high temperatures. To be more explicit, this pertains to the case when \( \gamma = \frac{E_k T q V_m B}{(2)} \) (see Supplemental Information for a detailed derivation). In this case, Eq. (7) reduces to:

\[
I = \frac{2q}{h} \frac{\gamma L \gamma R}{\gamma_L + \gamma_R} \left( \frac{q V}{k_B T} \right) e^{-E/F/k_B T}.
\]

The current in this case shows an activation behavior, with the "activation energy" \( \varepsilon \) being the offset between the energy level in the molecule and the Fermi energy in the leads. Note that a similar behaviour is expected from classical Marcus charge transfer processes, for which the activation energy has a completely different origin, as described above. We note that the activation energies arising from these two very different mechanisms may display different dependencies on the electric potentials applied to the junction, which therefore become powerful diagnostic tools to discern charge transport mechanisms. From Eq. (12) it follows that the activation energy \( \varepsilon \) would decrease with increasing bias voltage, as the electrostatic potential of the lead approaches the molecular level. This does not need to be the case in, e.g., polaron-assisted conduction, where polarization of neighbouring molecules may be affected by the applied bias in intricate ways, resulting from its direct effect on the polaron dynamics.

Figure 3 shows tunneling calculations using Eqs (5) and (7), to solve for the electrical current through a single molecular level described with the following characteristic parameters: \( \varepsilon = 0.4 \text{ eV} \), \( \eta = 0.5 \), and \( V_g = 0 \).
\[ \gamma_L = \gamma_R = 1 \text{ meV} \] (in Fig. 3a–c) and 10 meV (in Fig. 3d) and with different bias voltages: \( V \in 0.4 - 0.7 \text{ V} \). As can be clearly seen, there are two distinct regimes: decaying and saturated currents. The temperature of the transition between the two regimes (namely, the inflexion point where the plateau starts to develop) depends on the bias voltage: the lower the bias the higher the transition temperature (compare Fig. 3a–c). The same correspondence is observable for the slope in the thermally activated regime. As determined from Eq. (12), the “activation energy” decreases with increasing bias (since the separation \( \varepsilon \) between the molecular level and the electrochemical potential of the leads decreases with increasing bias). In addition, one can observe that increasing the level width smears out the difference between the two regimes (compare Fig. 3b,d). Important for our discussion is the fact that one can explain temperature-dependent electrical conductance in a molecular junction with the same functionality (exponential) and within the common temperature range of existing experiments without the need for a thermal activation derived from Marcus-like energy relaxation processes in the molecules (also possible but less likely in many solid state junctions). Indeed, this approach was successfully employed to explain the temperature dependence of the conductance through an individual sulfur end-functionalized terephthaloyldiene molecule in a SET device by van der Zant and collaborators in 200637. In that case, the width of the molecular level had to be adjusted for different bias voltages, from a few meV at low bias up to 30 meV as the system was brought into resonance at large bias. As discussed above, this effect can be understood in terms of a broadening of the molecular level width as a result of internal molecular vibrations excited by the increasing current when the system is brought closer to resonance.

Three-terminal single-electron transistor measurements of a Ferrocene-based junction. Figure 4a shows the electrical current at \( T = 80 \text{ K} \) as a function of gate voltage for a bias of \( V = 10 \text{ mV} \) through an individual S-(CH\(_2\))\(_4\)-Fc-(CH\(_2\))\(_4\)-S molecule placed in between the leads of an electromigrated three-terminal Al\(_2\)O\(_3\)/Au SET (see sketch in Fig. 4) fabricated according to the procedure given in ref. 44. Two peaks in the current are clearly visible at \( V = +0.3 \text{ V} \) and +1.7V. These peaks separate three consecutive charge states (\( N = -1, 1, \) and \( N = 1\) of the molecule, when no current is allowed to flow at low bias (i.e., Coulomb blockade). Details of the transport results and the synthesis of the molecule are given in ref. 45. From \( V \) vs. \( V - V_c \) measurements, the actual separation between these two charge points is 160 meV, from which we extract a gate capacitance factor (i.e., \( V_c = CV \)) of \( \varepsilon = 0.08 \). The data in Fig. 4a (solid black circles) can be well resolved (continuous red line in Fig. 4a) using the single-level model in Eq. (7) including two conduction levels (1 and 2) with the following characteristic parameters: \( \varepsilon_1 = -25 \text{ meV}, \varepsilon_2 = 135 \text{ meV} (\varepsilon_1 - \varepsilon_2 = 0.160 \text{ eV}), \eta = 0.5, \gamma_2 = 0.02 \text{ meV} \) and \( \gamma_1 = 0.06 \text{ meV} \).

The measurement in Fig. 4a was repeated at different temperatures up to \( T = 220 \text{ K} \). The behavior of the tunnel current with temperature is shown in Fig. 4b for four different gate voltages (\( V_g = -1.5, -0.7, -0.3, \) and 0.9 V) characteristic of the different conduction regimes in this junction, as indicated by the arrows in Fig. 4a. The agreement with the theoretical expectation is significant for all voltages, whether the conduction is in the Coulomb blockade regime (\( V_g = -1.5 \text{ and } +0.9 \text{ V} \)) or in the transport regime (\( V_g = -0.7 \text{ and } -0.3 \text{ V} \)).

The inset to Fig. 4b shows fits of current against inverse temperature, from which one can clearly discern the overall behavior for the different conduction regimes, including the transition into a temperature independent regime (quantum coherent plateau) at sufficiently low temperatures. Both the transition temperature and the “activation energy” depend on the gate voltage, as expected from Eq. (12) and discussed above.

We note that the same temperature behaviour has been observed in several other studies of this family of ferrocene-based molecules in EGaIn junctions45, illustrating the robustness of the theoretical analysis used in this work to determine the characteristic parameters of solid-state molecular junctions, and serving as a contextualization for the following theoretical analysis of experiments performed in SAM-based molecular junctions.

A two-level SAM-based molecular junction. Let us focus now on some very recent experiments in SAM-based molecular junctions where a record-high rectification ratio of three orders of magnitude has been achieved32. Figure 5 shows the sketch of a molecular junction formed by a SAM of (CH\(_2\))\(_3\)-Fc\(_2\) molecules (with Fc\(_2\) representing a biferrocenylene (Fc = Fc) head group) sandwiched in between GaO\(_{x}\)/EGaIn (top) and Ag (bottom) electrodes (see refs 22,46 for synthesis and experimental details). In these junctions, the Fc\(_2\) lies at the end of a long insulating alkyl chain, providing a non-covalent contact (van der Waals coupling) to the top electrode. This results in a highly asymmetric drop of electric potential at both sides of the Fc\(_2\) (where the frontier orbitals are located) enabling large rectification ratios. In particular, the Fc\(_2\) presents two distinct conduction levels (HOMO and HOMO-1 levels subsequently entering the conduction window defined by the difference in electrochemical potential of the top and bottom electrodes).

These results can be easily explained by incorporating a second level into the single-level transport model to account for the two Fc\(_2\) levels, i.e., the HOMO and the HOMO-1. Specifically, the addition of two different Lorentzian functions, as given in Eq. (6), weighted by the corresponding tunneling rates is used in Eq. (7) to represent the two contributing levels. The results of the calculation using Eq. (7) are shown in Fig. 5 (continuous red line) for the following characteristic parameters: \( \varepsilon_1 = 0.35 \text{ eV}, \varepsilon_2 = 0.75 \text{ eV}, \eta_1 = 0.95, \gamma_1 = 3 \text{ meV}, \gamma_2 = 1 \text{ meV}, \gamma_2 = 5 \text{ meV}, \gamma_2 = 2 \text{ meV} \). Note: the same results are obtained by Eq. (5) at room-temperature. The agreement is significant given the approximations in the model and the inherent degree of dispersion in the SAM-based molecular junctions. The theory recovers the voltage position of the two kinks, supporting their association with the
HOMO and HOMO-1 levels of the Fc2 group, as well as the overall value of the rectification for most of the bias voltage range, including the maximum rectification of three orders of magnitude. As discussed in ref. 22, the separation between the levels in the R-V plot (0.4 eV, Fig. 5) is smaller than that measured by CV and UPS (0.6 eV), which can be ascribed to an energy-renormalization of the molecular levels as a result of charge-image effects by the electrodes. This effect should also decrease the HOMO-LUMO gap (estimated to be >2 eV), allowing it to play some role in the conduction at large bias voltages (reverse polarity), which is likely responsible for the decrease of the rectification ratio above 1 V (see Fig. 5).

Given the fact that molecules are not all identically placed with respect to the electrodes and that their disposition may actually change during the course of a complete measurement, we have used Gaussian distributions for the energies of the HOMO and HOMO-1 levels to account for the degree of dispersion in the system. To do so, we modify Eq. (7) as follows (note once again that Eq. (5) can be treated in the same way to give the same results at high temperature):

\[
I = \frac{q}{h} \int \int_{-\infty}^{\infty} dE' dE \frac{\gamma_L \gamma_R}{\gamma_L + \gamma_R} \left[ f_{L}(E) - f_{R}(E) \right] g_{E'}(E'),
\]

where,

\[
g_{E'}(E) = \exp \left( \frac{(E - \varepsilon)^2}{2W^2} \right)
\]

The best results are obtained for a width of the Gaussian distribution \(W = 0.04\) eV for each level (green line in Fig. 5). This small dispersion in the position of the energy of the molecular levels (<10%) is indicative of the high degree of electrical stability in these SAM-based molecular junctions.

Maximum rectification ratio for a single-level junction. We note that the rectification ratio of three orders of magnitude observed for this molecular junction (with typical level widths \(\gamma \sim 1-10\) meV) is at the theoretical maximum limit expected from a single-level transport mechanism for characteristic positions of the frontier orbital with respect to the Fermi energy (\(\varepsilon \sim 0.5-1\) eV) and operating voltages (\(V \sim 1\) volt). This is easy to deduce by looking in Fig. 6 at the current and rectification ratios calculated from Eq. (7) for a molecular junction, where the parameters have been chosen to be representative of these kinds of junctions (i.e., derived from experimental data). In particular, the calculations have been obtained for a single-level positioned at \(\varepsilon = 0.5\) eV, and with a maximally asymmetric voltage divider parameter \(\eta = 0\), to maximize the rectification ratio. Obviously, the rectification will be maximum for a bias voltage larger than \(-0.5\) V, which is the forward voltage needed to bring the molecular level into resonance when \(\eta = 0\) (as obtained from the definition of \(E_{m2}\) and illustrated in Fig. 2).

Figure 6a shows the behaviour of the room-temperature electrical current with \(\gamma_L\) (with \(\gamma_L = \gamma_R\)) for both polarities of the bias voltage (\(V = \pm 1\) volt). As expected, the difference between the forward and reverse currents increases as the tunneling rates (and consequently the level widths) decrease. Both currents reach the same saturation value at sufficiently high tunneling rates (i.e., \(\gamma \gtrsim 1\) eV), when the level width is larger than the separation...
between electrochemical potentials in the leads and the conductance becomes constant, as discussed above. The corresponding $R$ for these voltages is shown in Fig. 6b for different temperatures, to emphasise that it does not vary below room-temperature. In the range $10^{-5} < \gamma_i \lesssim 1 \text{ eV}$ the electrical rectification decreases exponentially at room-temperature and below, saturating at $R = 1$ (no rectification) for $\gamma_i \gtrsim 1 \text{ eV}$, corresponding to the behaviour of the current in Fig. 6a. From these results one can conclude that in molecular junctions of this kind, where the $\gamma_i$ takes values typically above 1 meV, the rectification ratio will be limited to three orders of magnitude when a single electrostatic molecular level contributes to the conductance through the junction, which is the value found in the experiments reported in ref. 22 and marked by the arrows in Fig. 6.

We want to stress again that this result is found for voltage conditions that maximize the rectification efficiency (i.e., $\eta = 0$) but with an experimentally relevant energy location of the frontier orbital ($\varepsilon = 0.5 \text{ eV}$) and typical values of $\gamma_i$. Larger $\varepsilon$ values and, consequently, larger voltages will increase this limit, but not substantially. Evidently, if more than one molecular level is involved in charge transport the rectification can be improved by a factor proportional to the total number of levels involved. However, since it is unlikely to find molecular junctions with more than a few levels in the vicinity of the electrochemical potential of the leads, it is wise to expect substantially higher electrical rectification ratios originating from the molecular level structure. Imaginative ways should be explored in order to overcome this limit in practice, perhaps by engineering junctions that mix high single-level rectification properties with conformational changes in the molecule that can build up to increase the overall rectification of the junction.

**Determination of the electrostatic potential profile in a molecular junction.** Some of the authors in this article have recently reported a study of electrical rectification in EGaIn SAM-based junctions where the Fc unit was placed at 14 different positions within the SAM. The molecules have the form of $S-$C$_n$-Fc-C$_{13-n}$, where C$_n$ represents the number of aliphatic carbons (CH$_2$ or a terminal CH$_3$), with $n = 0$ to 13$^{33}$. Controlling the position of the Fc unit (where the molecular HOMO level is localized) along the alkyl chain for different values of $n$ (see sketches in Fig. 7) allows us to quantify the rectification response for different energetic symmetries in the junction (values of $\eta$), since the electric potential at both sides of the conduction unit (i.e., Fc) will strongly depend on its position along the chain. This enables sampling of the electrostatic potential profile along the junction gap, which was found to be highly non-linear in this particular molecular junction$^{33}$. 

![Figure 6. Limits on Molecular Tunneling Rectification.](image-url)

(a) Electrical current and (b) rectification ratio as a function of $\gamma_i$ (with $\gamma_L = \gamma_R$) calculated solving Eq. (7) for a single-level molecular junction with the following parameters: $\varepsilon = 0.5 \text{ eV}$ and $\eta = 0$. For the typical smallest values of $\gamma_i = 1 \text{ meV}$, the rectification originated from a single level (e.g., the HOMO orbital) in a molecular junction is theoretically limited to about three orders of magnitude.
Figure 7 shows $R$ as a function of $n$ measured at room-temperature and calculated by comparing the electrical currents at $V = \pm 1$ V. As can be clearly observed, the rectification behavior is highly non-linear, with several distinct areas, and with the maximum rectification values achieved when the Fc unit is placed close to one of the electrodes (i.e., $n = 3$ and $n > 10$), as expected from the asymmetry in the potential drops at both sides of the Fc. For $n < 3$ the strong hybridization between the Fc and the bottom electrode (chemisorbed contact) leads to large level broadenings and leakage currents, which in turn results in lower rectification ratios (see ref. 33 for more details). A similar effect (i.e., $R$ saturates), although weaker, arises for $n > 10$ due to proximity to the top electrode, where the coupling between the molecule and the lead is non-covalent (van der Waals interactions). The intermediate range of Fc positions ($4 < n < 11$) is the most interesting in the context of the analysis of the electrostatic potential profile in this article, since coupling between the Fc unit and the electrodes is non-covalent, and the molecular level responsible for conduction is well defined, with a width that can be considered constant, as we discuss below.

The results in Fig. 7 have been fitted to the single-level model given in Eq. (7) with characteristic energy parameters defined in the following. We reiterate once again that Eq. (5) will give the same exact results for this temperature and electric potential conditions. Before getting into the details of the calculations, we emphasise that the fitting results show that the distinct behaviour of $R$ for intermediate $n$ values, and particularly its small slope for $n = 5–9$ (Fig. 7), can only be explained by taking into account screening effects, i.e., a non-linear electrostatic potential profile. As we show below, single-level transport models together with a functional treatment to account for electric field screening proposed by Nitzan and collaborators allows determination of the electrostatic potential profile and extraction of a quantitative estimate of the screening length in a molecular junction, which has not been possible to date.

In the following we describe the analytical models that have been employed to fit the rectification data in Fig. 7 by means of Eq. (7). First, for the distance dependence of the energy of the HOMO level, $\varepsilon$, the following “synthetic” function has been employed: $\varepsilon(n) = \varepsilon(n \sim 13) - Ae^{-bn}$, with $\varepsilon(n \sim 13) = 0.75$ eV (see solid black line in Fig. 8b). The rationale behind this selection is based on the $n$-dependence of $\varepsilon^{\text{exp}}$ obtained from UPS data (see solid data in Fig. 8a), which departs from its linear behavior for distances below $n \sim 5$. The solid black squares in Fig. 8b, closely following the function used in the calculations (solid black line), represent the result of subtracting a linear function (dashed line in Fig. 8a) from the experimentally obtained value of $\varepsilon^{\text{exp}}$. The linear behavior is associated with screening by the metallic electrodes and depends on the Fc-distance (thus the linearity). Therefore, for $n > 5$ the energy offset $\varepsilon(n)$ is expected to be constant (i.e., independent of $n$). Departures from linearity (as observed for $n < 5$) are ascribed to a real change in the distance between the molecular level and the Fermi energy of the electrode, which in this case decreases. Figure 8b shows the experimental data of Fig. 8a after subtraction of the linear slope (black squares), together with the function used to fit the data (black line).
Distance-dependence functions have been chosen to represent the coupling energies $\gamma_{LR}(n)$ and $\gamma_{RL}(n)$, and consequently the HOMO level width $\gamma(n) = \gamma_{LR}(n) + \gamma_{RL}(n)$, and $\varepsilon(n)$ in order to account for the effect of the coupling to the respective electrodes. Figure 8b shows the values of $\gamma(n)$ and $\varepsilon(n)$ used in the calculations (solid curves). The broadening of the HOMO level in proximity with the electrode is expected to increase exponentially with decreasing Fc-electrode distance. Fermi’s golden rule gives $\gamma_{LR}(n) = t_{LR}^2/D_{LR}(n)$, where $t_{LR}$ is the effective coupling matrix and $D_{LR}(n)$ the electron bandwidth in the electrodes. In general, $\gamma_{LR}(n) \propto e^{-k D_{LR}(n)}$, where $k$ is the tunneling attenuation coefficient, proportional to $\sqrt{E_{\text{barrier}} - E_F}$, which for alkyl chains on Au or Ag is on the order of a few eV. As can be observed in Fig. 8b, the functions chosen to mimic this effect for $\gamma_{LR}$ and $\gamma_{RL}$ are not purely exponential with $n$ close to the electrodes but saturate for distances below two CH2 units ($n < 2$ and $n > 12$) from the respective electrodes. This fitting is based on the spectroscopic data that shows little differences observed in the spectroscopic results between SAMs with $n = 0$ and 1 (and 2 to some extent). As shown in Fig. 8b (red curve), the used dependence for the level width reaches maximum values of $\gamma_{LR}(n < 2) = 360$ meV (due to strong hybridization with the Ag electrode) and $\gamma_{RL}(n > 11) = 40$ meV, and a base value of $\gamma = 30$ meV (with $\gamma_{LR} = \gamma_{RL} = 15$ meV) for intermediate distances, as obtained from the fitting of the rectification curves (see below). Note that taking the full width at half maximum from UPS data to estimate the molecular level broadening results in an overestimation of $\gamma$ due to limitations of the technique (see ref. 33 for details) and therefore we only can derive the relative values of $\gamma$.

According to Eqs (5) and (7), the only other ingredient for calculating the electrical current through the molecular junctions is the functional describing the electrostatic potential profile in the junction, which is represented by $\eta(n)$. We have used two different models to obtain this parameter: (i) A simple linear electrostatic potential profile; and, (ii) a correction to account for electrical screening in the alkyl chain. 

**Linear electrostatic potential profile.** Assuming a linear dependence of the voltage drop as a function of the distance between the Fc and the respective electrodes (i.e., $V_L \propto L_3$), one can rewrite $\eta = V_{LR}/(V_L + V_R)$ as $\eta \approx L_R/(L_L + L_R)$. To account for the voltage drop at the Fc, the expression above can be rewritten assuming a correction $L_{R_{\text{shift}}}$ for the respective lengths, and the expression for the dimensionless division parameter is:

$$\eta(L_R) = \frac{L_R + L_{FC}}{L_L + L_R + 2L_{FC}} + \eta_{\text{shift}},$$

(14)

where $\eta_{\text{shift}}$ is an effective shift introduced to account for the asymmetry generated by different couplings of the molecule with the two different electrodes and to explain the small rectification ratios ($R < 2$) observed in equivalent alkyl chains without the Fc unit, or when the Fc is placed in the middle of the chain. The corresponding $\eta$ in the case of our molecule is given in Fig. 9 (dashed purple line). Note that $8.7\% \approx L_R/(L_A + 2L_E)$ of the voltage...
drops in the Fc and remains unavailable for use in the rectification process. We note that the strength of this correction is proportional to the size of the active unit employed to sample the electrostatic potential profile, which in our case is substantially larger than the adjacent CH\textsubscript{2} units. An ideal unit to sample the electrostatic profile would be one of negligible size (which is not possible, of course). That would also guarantee that the sampled molecule would remain undistorted when moving the active unit within the chain.

The resulting rectification curve obtained using the linear model defined by Eq. (14) (dashed purple line in Fig. 7) does not give an overall good fit to the data but can explain some features. It quantitatively explains the high rectification ratios for 2 < n < 5 and n > 9 and accounts for the abrupt decrease of rectification for n < 3 (resulting from a substantial level broadening due to hybridisation with the left and right electrodes, which leads to a small rectification even in the absence of the Fc unit (or when it is placed at the center of the junction). The linear profile that would be expected in vacuum (red curve) is modified when accounting for electrical screening by the alkyl chain, idealized as a cylinder of diameter \( \sigma \) and electrical screening length \( \lambda \).

**Correction for the screening of the electric field by the molecule.** The electrochemical potential in electrode-conductor-electrode junctions drops mainly at the contacts, but this is not applicable to the electrostatic potential, which may show profiles extending well into the low-dimensional conductor (e.g., molecule) for sufficiently long electric screening lengths, \( \lambda \), which is the case in semiconductors and molecular insulators (see Liang et al.\textsuperscript{48} and references therein for a more detailed discussion). It is therefore necessary to account for electrical screening effects when trying to explain our observations. For this, we have followed the theoretical formalism developed by Nitzan et al.\textsuperscript{47}, in which the molecule is approximated by a cylindrical conductor of diameter \( \sigma \), and electric field screening length \( \lambda \). As discussed by the authors, the screening length in molecular conductors is an open question, and systems with small HOMO-LUMO gaps are expected to screen well. Assuming that screening over the characteristic length of our system can be described by a Poisson formalism, the voltage division parameter describing the electrostatic potential profile can be written as:

\[
\eta(L_R) = \eta_0(L_R) + \frac{A}{\pi \sigma} \sum_{m=1}^{\infty} \frac{F_m}{m(1 + F_m)} \sin \left( \frac{2\pi m}{L_L + L_R} \right) + \eta_{\text{shift}},
\]

where \( \eta_0(z) \) is the linear profile given in Eq. (14). \( A \) is a factor to correct for the voltage drop in the Fc. The coefficients \( F_m \) can be expressed analytically as:

\[
F_m = \frac{1}{2} \left( \frac{\sigma}{\lambda} \right)^2 \int_{\lambda}^{\sigma} du e^{-u^2},
\]

with,

**Figure 9. Electrostatic Potential Profile: Theory.** Electrostatic potential profiles in the molecular junctions as represented by the dimensionless voltage division parameter \( \eta \). The curves represent the voltage drop within the alkyl chain on both sides of the Fc unit (totalling 91.3%), which is not the total voltage drop in the junction, since a substantial fraction decays in the Fc (8.7%). Also, the curves have been shifted from \( \eta = 0.5 \) in order to account for the different binding energies of the molecule with the left and right electrodes, which leads to a small rectification even in the absence of the Fc unit (or when it is placed at the center of the junction). The linear profile that would be expected in vacuum (red curve) is modified when accounting for electrical screening by the alkyl chain, idealized as a cylinder of diameter \( \sigma \) and electrical screening length \( \lambda \).
Using $\eta = 2.38 \, \text{Å} (=0.125(L_u + L_d))$, which is taken as the effective diameter of the alkyl chain, the electrostatic potential profiles for different screening lengths ($\lambda = 0.95, 1.50, 1.90$ and $2.85 \, \text{Å}$) are shown in Fig. 9. It can be clearly observed that the departure from linear behavior is more pronounced as the screening length decreases. In the limit $\lambda \to 0$, the electrostatic potential will follow the electrochemical potential and drop entirely within the vicinity of the contacts.

The results of the corresponding fittings of the rectification data are shown in Fig. 7 for three screening lengths: $\lambda = 1.30 \, \text{Å}$ (black line), $\lambda = 1.50 \, \text{Å}$ (blue line) and $\lambda = 1.90 \, \text{Å}$ (green line). From the good quantitative agreement with the experimental results, where the small slope in the rectification ratio can be well accounted for at intermediate values of $n$, one can estimate the characteristic screening length to be approximately $\lambda = 1.50 \pm 0.2 \, \text{Å}$. These values of the screening length are comparable to the molecular diameter $\sigma$, indicating that the electric field lines from vacuum penetrate well into the molecule.

Discussion

We have shown the validity of a simple but formal analytical single-level tunneling model that uses input parameters to calculate $I(V)$ curves that can be experimentally obtained (tunneling rate $\gamma$, the dimensionless division parameter $\eta = \frac{V_{th}}{(V_1 + V_2)}$, and the zero-bias energy offset between the molecular orbital and the electrodes $\varepsilon$). This model was tested against a well-characterized molecular diode and faithfully recovered the rectification ratio and the temperature dependent behavior of the junctions, from which we conclude that it is applicable to describe transport data from both single molecule and SAM-based junctions where intra-molecular collective behavior does not significantly affect the electronic structure of the junction.

One of the main conclusions from our theoretical treatment of the rectification ratio is that the highly non-linear electrostatic potential profile in typical molecular tunneling junctions is the result of a sizeable screening length in the molecule ($\lambda = 1.50 \pm 0.2 \, \text{Å}$, for ferrocene-alkanethiol). Fitting our equations to the experimental results shows that the electrostics of the molecular junction may be sampled simply by placing the redox Fc unit at different positions along the junction. These results confirm the expectation that potential profiles in insulating molecules are neither linear (as in vacuum) nor do they follow the electrochemical potential profile, which would lead to flat profiles within the entire length of the molecule and would prevent the attainment of high rectification ratios by capacitive coupling with the active transport unit. It is important thus to identify molecular ligands that provide long screening lengths in order to achieve linear-like potential profiles and extend the range of lengths for which the molecular diode would be an efficient rectifier of electrical current.

In addition, we have shown that simple single-level transport models (to describe incoherent and coherent tunneling) can account for the typical temperature dependencies of the conductance in solid state junctions and provide a powerful analysis tool to extract the characteristic parameters governing tunneling in these junctions in a consistent way.

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Author Contributions

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Author Contributions

A.R.G. performed the single-electron transport measurements, L.Y. and L.W. synthesized and characterized the SAMs, and performed the J(V) measurements of the SAM-based junctions discussed in the article. E.R.M. described the formal theoretical treatment employed in the analysis of the experimental results (included in the supplementary information). D.T. assisted in the interpretation of the results. E.d.B. and C.A.N. supervised the project. All the authors contributed to writing the manuscript.

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