Plasmon Scattering from Single Subwavelength Holes

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We map the complex electric fields associated with the scattering of surface plasmon polaritons by single subwavelength holes of different sizes in thick gold films. We identify and quantify the different modes associated with this event, including a radial surface wave with an angularly isotropic amplitude. This wave is shown to arise from the out-of-plane electric dipole induced in the hole, and we quantify the corresponding polarizability, which is in excellent agreement with electromagnetic theory. Time-resolved measurements reveal a time delay of \(38 \pm 18\) fs between the surface plasmon polariton and the radial wave, which we attribute to the interaction with a broad hole resonance.

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The interaction of light, and, in particular, of surface waves such as surface plasmon polaritons (SPPs), with subwavelength holes in metallic films leads to phenomena such as extraordinary optical transmission [1,2] and negative index metamaterials [3–6]. In this context, subwavelength holes are important in diverse fields of research, such as nanophotonics, enhanced nonlinear optics, and biosensing, and consequently, with a few notable exceptions [7,8], experiments focus on the macroscopic consequences of the light-hole interactions. Conversely, much theoretical work has been devoted to their understanding from a microscopic viewpoint [9–12]. That is, while the models intrinsically consider scattering of light and SPPs from subwavelength defects, often in terms of their polarizabilities, most experimental studies address collective response features such as extraordinary optical transmission spectra and their dependence on changes in sample geometry, film thickness [13], and hole shape [14]. In essence, a detailed investigation of the dynamics of plasmonic scattering remains incomplete.

In this Letter, we present a systematic experimental study of the scattering of SPPs from individual circular subwavelength holes of different diameters in optically thick gold films. We use phase-sensitive time-resolved near-field optical observations to measure the plasmonic scattering on a nanometer length and femtosecond time scale, determining the angularly resolved scattering amplitude for subwavelength holes of different sizes and quantifying the temporal dynamics of the scattering events. We show that these results can be explained in terms of the polarizability of the hole, in excellent agreement with electromagnetic theory.

We investigate the scattering from individual holes, with diameters ranging from 50 to 980 nm, milled with a focused ion beam into a 200 nm thick gold film deposited on a glass substrate. We launch SPPs on the air-gold interface by illuminating a slit in the film with either 150 femtosecond FWHM pulses or a continuous wave laser source centered at a wavelength of 1550 nm. At this wavelength, a waveguide mode is supported by holes with diameters above 760 nm. These SPPs are efficiently directed towards the hole by a Bragg grating that is milled into the film on the opposite side of the slit [15], as shown in Fig. 1. We measure the complex electric field of this system, at a height of 20 nm, with near-field microscopy [16].

In Fig. 2, we present typical experimental results for a hole with a diameter of 875 nm. We observe fringes in the amplitude that originate from the interference of the forward propagating SPP with the scattered waves. Here, the dark vertical stripes near 5 and 8 µm are attributed to geometrical imperfections in the area of the launching slit. The salient features of the data are reproduced by first-principle calculations [Fig. 2(b)] performed by using a modified version of a model presented elsewhere [12]. This method, which involves a rigorous expansion of Maxwell’s equations, both in terms of plane waves on either side of the film and in cylindrical waves inside the hole, is used to calculate the electric and magnetic

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polarizabilities of the hole, which are in turn used to obtain the scattered fields [17].

The different waves present in the scattering event are readily identifiable in $k$ space [18] after a Fourier transform [Fig. 2(c)]. In $k$ space, signatures of the forward propagating SPP, evidenced by the peak near $2\pi$, and the scattered wave, which emerges as a circular pattern, are readily separable. These signatures are shown in Fig. 2(d), in which both the data (thick shaded curves) and the fits for the different surface waves (thin dark curves) are presented. The distributions of both waves peak around a wave vector $k = 4.2$ $\mu m^{-1}$, which is in good agreement with the theoretical value of $k_{\text{sp}} = k_0 \sqrt{\varepsilon/(\varepsilon + 1)} = 4.1$ $\mu m^{-1}$, obtained from the dielectric constant of gold at 1550 nm, $\varepsilon = -115 + 11i$ [19].

In the inset in Fig. 2(d), we show the angular dependence of the in-plane electric field distribution. Here, the outer curve represents the total integrated field amplitude, while the inner curve represents the integrated amplitude that we can attribute to the surface waves. We find these curves by integrating up to $k = 5.0$ $\mu m^{-1}$ under the data and fits, respectively, in each direction (main part of the figure).

First, we observe no angular dependence of the radial mode and attribute the slight left-right asymmetry found in our measurements to either a slightly asymmetric hole or near-field tip. Second, for this relatively large hole the amplitude content of the radial wave is about 7% of the amplitude of the forward propagating SPP. As we show below (Fig. 5), for an 875 nm hole 0.7 of the forward propagating SPP amplitude is contained in the incident...
beam, and hence the amplitude of the radial wave is \(\sim 10\%\) that of the incident SPP. Note that our incident Gaussian beam is \(\sim 6\ \mu m\) width, which is larger than the hole (see [17] for a discussion on the scattering cross section of the hole). Finally, from these data we can also estimate that approximately half of the radially scattered field amplitude is in the surface modes. The remaining half of the radial fields have in-plane wave vectors that are smaller than \(k_0 = 2\pi/\lambda = 4.05\ \mu m^{-1}\), corresponding to radiative modes of light, which propagate upward, away from the metal surface. Qualitatively, these are seen as the regions of nonzero amplitude within the surface wave circle in Fig. 2(c) or in the difference between the inner and outer curves (other than near \(0^\circ\)) in Fig. 2(d).

In order to determine the nature of the detected scattered field, we consider its asymptotic form [17]

\[
(E_x, E_y, E_z) = 2k_0^2 \left(\frac{2\pi}{k_{sp} R}\right)^{1/2} \left(\frac{\epsilon}{1 + \epsilon}\right)^2 \left(1 - \frac{1}{1 + \epsilon}\right) e^{-2\pi(i/4)k_{sp} R + w_{sp} z} \times A^{sc}(\varphi) (-w_{sp} \hat{R} + k_{sp} \hat{z}),
\]  

(1)

where the azimuthal scattering amplitude

\[
A^{sc}(\varphi) = -p_x \cos \varphi - \sqrt{1 + \epsilon} m_y \cos \varphi + \sqrt{\epsilon} p_z
\]

(2)
is given for excitation by a SPP that travels along the \(x\) direction. Here, \(R\) is the in-plane radial distance to the hole center, \(z\) is the height above the film surface, \(w_{sp} = -k_0/\sqrt{(\epsilon + 1)}^{0.5}\) is the out-of-plane component of the SPP wave vector, \(\hat{z}\) and \(\hat{R}\) are out-of-plane and in-plane unit vectors, respectively, \(p_x\) and \(p_z\) are the in- and out-of-plane electric dipoles, respectively, and \(m_y\) is the in-plane magnetic dipole of the hole. Consequently, the isotropic nature of the detected scattered field [inset in Fig. 2(d)] suggests that we are mostly sensitive to the contribution from \(p_z\). This is not entirely unexpected, since the contributions of other dipole components peak near \(\varphi = 0^\circ\) and \(180^\circ\) and are therefore hard to separate from the incident SPP field. However, we note that to accurately reproduce the field in all directions [Fig. 2(b)] the fields that arise due to \(m_y\), as well as those due to \(p_z\), are required [17].

We image the \(p_z\)-dependent electric field by filtering out the forward propagating SPP mode in \(k\) space and then Fourier transforming back to real space. In Fig. 3, we show this field both near \(\varphi = -90^\circ\), where only a contribution from \(p_z\) is expected, and in a \(400\ \mu m^2\) area around the hole (inset). A fit of the form \(\exp(ikR)^{-a}\) reproduces the experimental data with \(k = 4.20 \pm 0.02\ \mu m^{-1}\) and \(a = 0.57 \pm 0.10\). Hence, the measured amplitude damping is in excellent agreement with the \(1/\sqrt{R}\) behavior predicted for circular waves by Eq. (1), as required for energy conservation for radial propagation on a plane. The discrepancy between the data and fit close to the hole may be indicative of the presence of creeping waves, which can have substantial amplitudes at short distances [9]. We can also use Eq. (1) to express the ratio of the scattered field to the incident field for \(\varphi = 90^\circ\) in terms of the electric polarizability

\[
\frac{A^{sc}}{A^{in}} = 2\sqrt{2\pi} \left(\frac{e}{1 + e}\right)^2 \left(\frac{e}{1 - e}\right)^2 k_0^2 w_{sp} \alpha_E.
\]

(3)

Hence, we measure \(|\alpha_E| = (4.1 \pm 0.1) \times 10^{-21}\ \text{m}^3\), which is larger than, but comparable to, the value \(|\alpha_E| = 3.3 \times 10^{-21}\ \text{m}^3\) calculated for a hole in a perfectly conducting film [17].

In Fig. 4, we present the temporal dynamics of plasmonic scattering, showing the amplitudes of both the forward and scattered radial modes as a function of time. The forward amplitude is averaged over a range of \(\pm 5^\circ\), while the scattered amplitude is averaged over a similar range in the transverse directions (\(\theta = \pm 90^\circ\)) to ensure no overlap between the modes. Both amplitudes are normalized to the peak of the forward propagating SPP, and the second peak of the double peak results from SPPs that are initially launched backward and subsequently reflect from the Bragg grating towards the hole [15]. Most strikingly, we observe that the radial wave peaks one time step after the forward propagating SPP. There is a time delay between the forward propagating SPP pulse and the radial pulse resulting from the plasmonic scattering. By averaging over the time delay that we measure between the incident SPP and the scattered wave, in all available directions, we quantify this shift as \(38 \pm 18\ \text{fs}\). While the frequency dependence of the polarizability of the hole alone results in a shift only a few femtoseconds, it is
able to explain the observed shift when combined with a modestly chirped incident pulse. That is, since the different frequencies that form our pulse scatter from the hole with different amplitudes and phases, their reconstitution into a pulse results in the observed time shift. This shift, then, represents a first measurement of the complex spectral response of an individual hole.

We study the effect of hole size on the plasmonic scattering for hole sizes ranging from 50 to 980 nm. The results are summarized in Fig. 5. The inset depicts the fraction of the field amplitude that is contained in the forward propagating SPP mode, which we normalize to the field on films without a hole. As expected, less energy is found in this plasmonic wave as the hole size increases and hence scatters more energy.

The main part of Fig. 5 depicts the dependence of the scattered field amplitude of the radial wave normalized to that of the forward plasmon field (symbols) on the hole diameter $d$. This dependence is accurately reproduced by the calculated electric polarizability of the hole (curve) [17]. An offset of 0.017 is present in the data (and added in the calculations) due to measurement noise and represents a signal-to-noise ratio of about 50 to 1, while the error bar is mainly indicative of the asymmetry of our measurements. For the smaller holes, well below the cutoff, the field amplitude increases as $-d^3$, where the divergence from a perfect dipolar behavior is due to the finite size of the hole and the film thickness. As the hole size increases, and, in particular, once the cutoff is reached and waveguide modes in the hole become accessible, the scattered amplitude begins to saturate. We attribute this behavior to an increase in energy flow through the hole [17]. Finally, we note that the scattered amplitude peaks at about 10% of the forward propagating SPP amplitude.

In summary, we have captured the near-field interplay between the waves associated with plasmon scattering from subwavelength holes and mapped both their dependence on hole size and their temporal dynamics. We show that both the hole-size-dependent amplitude and the time delay of the scattered mode can be understood in terms of the calculated polarizability of the hole. Our results provide a comprehensive understanding of hole-plasmon scattering and should, in the future, allow for the optimization of the interaction between holes. Consequently, the geometric properties of hole arrangements can be tuned to create electromagnetic hot spots. These can be used to, for example, enhance emission from dye molecules, address individual quantum emitters, or create near-field distributions for sensing or imaging purposes. Hence, these results have implications for a broad range of nano-plasmonic applications.

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