Event generator tunes obtained from underlying event and multiparton scattering measurements

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Abstract New sets of parameters (“tunes”) for the underlying-event (UE) modelling of the PYTHIA8, PYTHIA6 and HERWIG++ Monte Carlo event generators are constructed using different parton distribution functions. Combined fits to CMS UE proton–proton (pp) data at \( \sqrt{s} = 7 \) TeV and to UE proton–antiproton (p\( \bar{p} \)) data from the CDF experiment at lower \( \sqrt{s} \), are used to study the UE models and constrain their parameters, providing thereby improved predictions for proton–proton collisions at 13 TeV. In addition, it is investigated whether the values of the parameters obtained from fits to UE observables are consistent with the values determined from fitting observables sensitive to double-parton scattering processes. Finally, comparisons are presented of the UE tunes to “minimum bias” (MB) events, multijet, and Drell–Yan (q\( \bar{q} \) \( \rightarrow \) Z/\( \gamma^* \) \( \rightarrow \) lepton-antilepton+jets) observables at 7 and 8 TeV, as well as predictions for MB and UE observables at 13 TeV.

1 Introduction

Monte Carlo (MC) event generators of hadron–hadron collisions based on perturbative quantum chromodynamics (QCD) contain several components. The “hard-scattering” part of the event consists of particles resulting from the hadronization of the two partons (jets) produced in the hardest scattering, and in their associated hard initial- and final-state radiation (ISR and FSR). The underlying event (UE) consists of particles from the hadronization of beam-beam remnants (BBR), of multiple-parton interactions (MPI), and their associated ISR and FSR. The BBR include hadrons from the fragmentation of spectator partons that do not exchange any appreciable transverse momentum \( (p_T) \) in the collision. The MPI are additional 2-to-2 parton-parton scatterings that occur within the same hadron–hadron collision, and are softer in transverse momentum \( (p_T \lesssim 3 \) GeV) than the hard scattering.

The perturbative 2-to-2 parton-parton differential cross section diverges like \( 1/p_T^4 \), where \( p_T \) is the transverse momentum of the outgoing partons in the parton-parton center-of-mass (c.m.) frame. Usually, QCD MC models such as PYTHIA [1–5] regulate this divergence by including a smooth phenomenological cutoff \( p_{T0} \) as follows:

\[
1/p_T^4 \rightarrow 1/(p_T^2 + p_{T0}^2)^2. \tag{1}
\]

This formula approaches the perturbative result for large scales and is finite as \( p_T \rightarrow 0 \). The divergence of the strong coupling \( \alpha_s \) at low \( p_T \) is also regulated through Eq. (1). The primary hard 2-to-2 parton-parton scattering process and the MPI are regulated in the same way through a single \( p_{T0} \) parameter. However, this cutoff is expected to have a dependence on the center-of-mass energy of the hadron–hadron collision \( \sqrt{s} \). In the PYTHIA MC event generator this energy dependence is parametrized with a power-law function with exponent \( \epsilon \):

\[
p_{T0}(\sqrt{s}) = p_{T0}^{ref}(\sqrt{s}/\sqrt{s_0})^\epsilon, \tag{2}
\]

where \( \sqrt{s_0} \) is a given reference energy and \( p_{T0}^{ref} \) is the value of \( p_{T0} \) at \( \sqrt{s_0} \). At a given \( \sqrt{s} \), the amount of MPI depends on \( p_{T0} \), the parton distribution functions (PDF), and the overlap of the matter distributions (or centrality) of the two colliding hadrons. Smaller values of \( p_{T0} \) provide more MPI due to a larger MPI cross section. Table 1 shows the parameters in PYTHIA6 [1] and PYTHIA8 [5] that, together with the selected PDF, determine the energy dependence of MPI. Recently, in HERWIG++ [6,7] the same formula has been adopted to provide an energy dependence to their MPI cutoff, which is also shown in Table 1. The QCD MC generators have other parameters that can be adjusted to control the modelling of the properties of the events, and a specified set of such parameters adjusted to fit certain prescribed aspects of the data is referred to as a “tune” [8–10].

In addition to hard-scattering processes, other processes contribute to the inelastic cross section in hadron–hadron collisions: single-diffraction dissociation (SD), double-diffraction dissociation (DD), and central-diffraction (CD).
Table 1 Parameters in PYTHIA6 [1], PYTHIA8 [5], and HERWIG++ [6,7] MC event generators that, together with some chosen PDF, determine the energy dependence of MPI

| Parameter | PYTHIA6 | PYTHIA8 | HERWIG++ |
|-----------|---------|---------|----------|
| MPI cutoff, $p_{T0}^{\text{eff}}$, at $\sqrt{s} = \sqrt{s_0}$ | PARP(82) | MultipartionInteractions:pT0Ref | MPIHandler:pT0Ref |
| Reference energy, $\sqrt{s_0}$ | PARP(89) | MultipartionInteractions:ccmRef | MPIHandler:ReferenceScale |
| Exponent of $\sqrt{s}$ dependence, $\epsilon$ | PARP(90) | MultipartionInteractions:ccmPow | MPIHandler:Power |

In SD and DD events, one or both beam particles are excited into high-mass color-singlet states (i.e. into some resonant N*), which then decay. The SD and DD processes correspond to color-singlet exchanges between the beam hadrons, while CD corresponds to double color-singlet exchange with a diffractive system produced centrally. For non-diffractive processes (ND), color is exchanged, the outgoing remnants are no longer color singlets, and this separation of color generates a multitude of quark–antiquark pairs that are created via vacuum polarization. The sum of all components except SD corresponds to non single-diffraction (NSD) processes.

Minimum bias (MB) is a generic term that refers to events selected by requiring minimal activity within the detector. This selection accepts a large fraction of the overall inelastic cross section. Studies of the UE are often based on MB data, but it should be noted that the dominant particle production mechanisms in MB collisions and in the UE are not exactly the same. On the one hand, the UE is studied in collisions in which a hard 2-to-2 parton-parton scattering has occurred, by analyzing the hadronic activity in different regions of the event relative to the back-to-back azimuthal structure of the hardest particles emitted [11]. On the other hand, MB collisions are often softer and include diffractive interactions that, in the case of PYTHIA, are modelled via a Regge-based approach [12].

The MPI are usually much softer than primary hard scatterers, however, occasionally two hard 2-to-2 parton scatters can take place within the same hadron–hadron collision. This is referred to as double-parton scattering (DPS) [13–16], and is typically described in terms of an effective cross section parameter, $\sigma_{\text{eff}}$, defined as:

$$\sigma_{\text{AB}} = \frac{\sigma_A \sigma_B}{\sigma_{\text{eff}}},$$

where $\sigma_A$ and $\sigma_B$ are the inclusive cross sections for individual hard scattering processes of generic type A and B, respectively, and $\sigma_{\text{AB}}$ is the cross section for producing both scatterers in the same hadron–hadron collision. If A and B are indistinguishable, as in four-jet production, a statistical factor of 1/2 must be inserted on the right-hand side of Eq. (3). Furthermore, $\sigma_{\text{eff}}$ is assumed to be independent of A and B. However, $\sigma_{\text{eff}}$ is not a directly observed quantity, but can be calculated from the overlap function of the two transverse profile distributions of the colliding hadrons, as implemented in any given MPI model.

The UE tunes have impact in both soft and hard particle production in a given pp collision. First, about half of the particles produced in a MB collision originate from the hadronization of partons scattered in MPI, and have their differential cross sections in $p_T$ regulated via Eq. (1), using the same $p_{T0}$ cutoff used to tame the hardest 2-to-2 parton-parton scattering in the event. The tuning of the cross-section regularization affects therefore all (soft and hard) parton-parton scatterings and provides a prediction for the behavior of the ND cross section. Second, the UE tunes parametrize the distribution in the transverse overlap of the colliding protons and thereby the probability of two hard parton-parton scatterers that is then used to estimate DPS-sensitive observables.

In this paper, we study the $\sqrt{s}$ dependence of the UE using recent CDF proton–antiproton data from the Fermilab Tevatron at 0.3, 0.9, and 1.96 TeV [11], together with CMS pp data from the CERN LHC at $\sqrt{s} = 7$ TeV [17]. The 0.3 and 0.9 TeV data are from the “Tevatron energy scan” performed just before the Tevatron was shut down. Using the RIVET (version 1.9.0) and PROFESSOR (version 1.3.3) frameworks [18,19], we construct: (i) new PYTHIA8 (version 8.185) UE tunes using several PDF sets (CTEQ6L1 [20], HERAPDF1.5LO [21], and NNPDF2.3LO [22,23]), (ii) new PYTHIA6 (version 6.327) UE tunes (using CTEQ6L1 and HERAPDF1.5LO), and (iii) a new HERWIG++ (version 2.7.0) UE tune for CTEQ6L1. The RIVET software is a tool for producing predictions of physics quantities obtained from MC event generators. It is used for generating sets of MC predictions with a different choice of parameters related to the UE simulation. The predictions are then included in the PROFESSOR framework, which parametrizes the generator response and returns the set of tuned parameters that best fits the input measurements.

In addition, we construct several new CMS “DPS tunes” and investigate whether the values of the UE parameters determined from fitting the UE observables in a hard-scattering process are consistent with the values determined from fitting DPS-sensitive observables. The PROFESSOR software also offers the possibility of extracting “eigentunes”, which provide an estimate of the uncertainties in the fitted parameters. The eigentunes consist of a collection of additional tunes, obtained through the covariance matrix of
the data-theory fitting procedure, to determine independent
directions in parameter space that provide a specific mod-
fication in the goodness of the fit, $\chi^2$ (Sect. 2). All of
the CMS UE and DPS tunes are provided with eigentunes.
In Sect. 4, predictions using the CMS UE tunes are com-
pared to other UE measurements not used in determining
the tunes, and we examine how well Drell–Yan, MB, and
multijet observables can be predicted using the UE tunes.
In Sect. 5, predictions of the new tunes are shown for UE
observables at 13 TeV, together with a comparison to the first
MB distribution measured. Section 6 has a brief summary
and conclusions. The appendices contain additional compar-
isons between the \textsc{pythia6} and \textsc{herwig++} UE tunes and the
data, information about the tune uncertainties, and predic-
tions for some MB and DPS observables at 13 TeV.

2 The CMS UE tunes

Previous UE studies have used the charged-particle jet with
largest $p_T$ \cite{24,25} or a Z boson \cite{11,26} as the leading (i.e.
highest $p_T$) objects in the event. The CDF and CMS data,
used for the tunes, select the charged particle with largest
$p_T$ in the event ($p_{\text{max}}^T$) as the “leading object”, and use just
the charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ to
characterize the UE.

On an event-by-event basis, the leading object is used to
define regions of pseudorapidity-azimuth ($\eta$-$\phi$) space. The
“toward” region relative to this direction, as indicated in
Fig. 1, is defined by $|\Delta \phi| < \pi/3$ and $|\eta| < 0.8$, and the
“away” region by $|\Delta \phi| > 2\pi/3$ and $|\eta| < 0.8$. The charged-
particle and the scalar-$p_T$ sum densities in the transverse
region are calculated as the sum of the contribution in the two
regions: “Transverse-1” ($\pi/3 < \Delta \phi < 2\pi/3$, $|\eta| < 0.8$) and
“Transverse-2” ($\pi/3 < -\Delta \phi < 2\pi/3$, $|\eta| < 0.8$), divided
by the area in $\eta$-$\phi$ space, $\Delta \eta \Delta \phi = 1.6 \times 2\pi/3$. The transverse
region is further separated into the “TransMAX” and “Trans-
MIN” regions, also shown in Fig. 1. This defines on an event-
by-event basis the regions with more (TransMAX) and fewer
(TransMIN) charged particles ($N_{\text{ch}}$), or greater (TransMAX)
or smaller (TransMIN) scalar-$p_T$ sums ($p_{\text{Trans}}^T$). The UE par-
ticle and $p_T$ densities are constructed by dividing by the area
in $\eta$-$\phi$ space, where the TransMAX and TransMIN regions
each have an area of $\Delta \eta \Delta \phi = 1.6 \times 2\pi/6$. The transverse
density (also referred to as “TransAVE”) is the average of the
TransMAX and the TransMIN densities. For events with hard
initial- or final-state radiation, the TransMAX region often
contains a third jet, but both the TransMAX and TransMIN
regions receive contributions from the MPI and beam-beam
remnant components. The TransMIN region is very sensitive
to the MPI and beam-beam remnant components of the UE,
while “TransDIF” (the difference between TransMAX and
TransMIN densities) is very sensitive to ISR and FSR \cite{27}.

The new UE tunes are determined by fitting UE observ-
ables, and using only those parameters that are most
sensitive to the UE data. Since it is not possible to tune all
parameters of a MC event generator at once, the para-
eters that affect, for example, the parton shower, the frag-
mentation, and the intrinsic-parton $p_T$ are fixed to the values
given by an initially established reference tune. The initial
reference tunes used for \textsc{pythia8} are Tune 4C \cite{28} and the
Monash Tune \cite{29}. For \textsc{pythia6}, the reference tune is Tune
Z2*lep \cite{25}, and for \textsc{herwig++} it is Tune UE-EE-5C \cite{30}.

2.1 The \textsc{pythia8} UE tunes

Taking as the reference tune the set of parameters of
\textsc{pythia8} Tune 4C \cite{28}, we construct two new UE tunes,
one using CTEQ6L1 (CUETP8S1-CTEQ6L1) and one using HERAPDF1.5LO (CUETP8S1-HERAPDF1.5LO). CUET (read as “cute”) stands for “CMS UE tune”, and P8S1 stands for PYTHIA8 “Set 1”.

The tunes are extracted by varying the four parameters in Table 2 in fits to the TransMAX and TransMIN charged-particle and \( \rho^\text{sum} \) densities at three energies, for pp collisions at \( \sqrt{s} = 0.9 \) and 1.96, and pp collisions at 7 TeV. The measurements of TransAVE and TransDIF densities are not included in the fit, since they can be constructed from TransMAX and TransMIN. The new tunes use an exponentially-falling matter-overlap function between the two colliding protons of the form \( \exp(-b \exp\text{Pow}) \), with \( b \) being the impact parameter of the collision. The parameters that are varied are \( \exp\text{Pow} \), the MPI energy-dependence parameters (Table 1) and the range, i.e. the probability of color reconnection (CR). A small (large) value of the final-state CR parameter tends to increase (reduce) the final particle multiplicities. In PYTHIA8, unlike in PYTHIA6, only one parameter determines the amount of CR, which includes a \( p_T \) dependence, as defined in Ref. [5].

The generated inelastic events include ND and diffractive (DD+SD+CD) contributions, although the UE observables used to determine the tunes are sensitive to single-diffraction dissociation, central-diffraction, and double-diffraction dissociation only at very small \( p_T^\text{max} \) values (e.g. \( p_T^\text{max} \sim 1.5 \) GeV). The ND component dominates for \( p_T^\text{max} \) values greater than \( \approx 2.0 \) GeV, since the cross section of the diffractive components rapidly decreases as a function of \( p_T \). The fit is performed by minimizing the \( \chi^2 \) function:

\[
\chi^2(p) = \sum_i \frac{(f^i(p) - R_i)^2}{\Delta_i^2},
\]

where the sum runs over each bin of every observable. The \( f^i(p) \) functions correspond to the interpolated MC response for the simulated observables as a function of the parameter vector \( p \), \( R_i \) is the value of the measured observable in bin \( i \), and \( \Delta_i \) is the total experimental uncertainty of \( R_i \). We do not use the Tevatron data at \( \sqrt{s} = 300 \) GeV, as we are unable to obtain an acceptable \( \chi^2 \) in a fit of the four parameters in Table 2. The \( \chi^2 \) per degree of freedom (dof) listed in Table 2 refers to the quantity \( \chi^2(p) \) in Eq. (4), divided by the number of dof in the fit. The eigentunes (Appendix A) correspond to the tunes in which the changes in the \( \chi^2 \) of the fit relative to the best-fit value equals the \( \chi^2 \) value obtained in the tune, i.e. \( \Delta \chi^2 = \chi^2 \). For both tunes in Table 2, the fit quality is very good, with \( \chi^2/\text{dof} \) values very close to 1.

The contribution from CR changes in the two new tunes; it is large for the HERAPDF1.5LO and small for the CTEQ6L1 PDF. This is a result of the shape of the parton densities at small fractional momenta \( x \), which is different for the two PDF sets. While the parameter \( \rho^\text{ref} \) in Eq. (2) stays relatively constant between Tune 4C and the new tunes, the energy dependence \( \epsilon \) tends to increase in the new tunes, as do the matter-overlap profile functions.

The PYTHIA8 Monash Tune [29] combines updated fragmentation parameters with the NNPDF2.3LO PDF.

The NNPDF2.3LO PDF has a gluon distribution at small \( x \) that is different compared to CTEQ6L1 and HERAPDF1.5LO, and this affects predictions in the forward region of hadron–hadron collisions. Tunes using the NNPDF2.3LO PDF provide a more consistent description of the UE and MB observables in both the central and forward regions, than tunes using other PDF.

A new PYTHIA8 tune CUETP8M1 (labeled with M for Monash) is constructed using the parameters of the Monash Tune and fitting the two MPI energy-dependence parameters of Table 1 to UE data at \( \sqrt{s} = 0.9 \), 1.96, and 7 TeV. Varying the CR range and the exponential slope of the matter-overlap function freely in the minimization of the \( \chi^2 \) leads to sub-optimal best-fit values. The CR range is therefore fixed to the value of the Monash Tune, and the exponential slope of the matter-overlap function \( \exp\text{Pow} \) is set to 1.6, which is similar to the value determined in CUETP8S1-CTEQ6L1.
Table 3 The PYTHIA8 parameters, tuning range, Monash values [29], and best-fit values for CUETP8M1, obtained from fits to the TransMAX and TransMIN charged-particle and \( p_T^{\text{sum}} \) densities, as defined by the leading charged-particle \( p_T^{\text{max}} \) at \( \sqrt{s} = 0.9, 1.96, \) and 7 TeV. The \( \sqrt{s} = 300 \) GeV data are excluded from the fit.

| PYTHIA8 parameter | Tuning range  | Monash       | CUETP8M1       |
|-------------------|---------------|--------------|----------------|
| PDF               | –             | –            | –              |
| MultipartonInteractions:pT0Ref [GeV] | 1.0–3.0      | 2.280        | 2.402          |
| MultipartonInteractions:cmcPow       | 0.0–0.4      | 0.215        | 0.252          |
| MultipartonInteractions:expPow       | –             | 1.85         | 1.6\(^a\)      |
| ColourReconnection:range       | –             | 1.80         | 1.80\(^b\)     |
| MultipartonInteractions:ecmRef [GeV] | –             | 7000         | 7000\(^b\) |
| \( \chi^2/dof \) | –             | –            | 1.54           |

\(^a\) Fixed at CUETP8S1-CTEQ6L1 value
\(^b\) Fixed at Monash Tune value

Fig. 2 CDF data at \( \sqrt{s} = 300 \) GeV [11] on particle (top) and \( p_T^{\text{sum}} \) densities (bottom) for charged particles with \( p_T > 0.5 \) GeV and \(|\eta| < 0.8\) in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle \( p_T^{\text{max}} \). The data are compared to PYTHIA8 Tune 4C, CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1. The ratios of MC events to data are given below each panel. The data at \( \sqrt{s} = 300 \) GeV are not used in determining these tunes. The green bands in the ratios represent the total experimental uncertainties.
The best-fit values of the two tuned parameters are shown in Table 3. Again, we exclude the 300 GeV data, since we are unable to get a good $\chi^2$ in the fit. The parameters obtained for CUETP8M1 differ slightly from the ones of the Monash Tune. The obtained energy-dependence parameter $\epsilon$ is larger, while a very similar value is obtained for $p_{T0}^{\text{ref}}$.

Figures 2, 3, 4 and 5 show the CDF data at 0.3, 0.9, and 1.96 TeV, and the CMS data at 7 TeV for charged-particle and $p_T^{\text{sum}}$ densities in the TransMIN and TransMAX regions as a function of $p_T^{\text{max}}$, compared to predictions obtained with the PYTHIA8 Tune 4C and with the new CMS tunes: CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1. Predictions from the new tunes cannot reproduce the $\sqrt{s} = 300$ GeV data, but describe very well the data at the higher $\sqrt{s} = 0.9$, 1.96, and 7 TeV. In particular, the description provided by the new tunes significantly improves relative to the old Tune 4C, which is likely due to the better choice of parameters used in the MPI energy dependence and the extraction of the CR in the retuning.

2.2 The PYTHIA6 UE tunes

The PYTHIA6 Tune Z2*lep [25] uses the improved fragmentation parameters from fits to the LEP $e^+e^-$ data [31], and a double-Gaussian matter profile for the colliding protons but corresponds to an outdated CMS UE tune. It was constructed by fitting the CMS charged-particle jet UE data at 0.9 and 7 TeV [24] using data on the TransAVE charged-particle and...
Fig. 4 CDF data at $\sqrt{s} = 1.96$ TeV [11] on particle (top) and $p_T^{\text{sum}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to PYTHIA8 Tune 4C, CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1. The ratios of MC events to data are given below each panel. The green bands in the ratios represent the total experimental uncertainties on $p_T^{\text{sum}}$ densities, since data on TransMAX, TransMIN, and TransDIF were not available at that time.

Starting with Tune Z2*lep parameters, two new PYTHIA6 UE tunes are constructed, one using CTEQ6L1 (CUETP6S1-CTEQ6L1) and one using HERAPDF1.5LO (CUETP6S1-HERAPDF1.5LO), with P6S1 standing for PYTHIA6 “Set 1”. The tunes are constructed by fitting the five parameters shown in Table 4 to the TransMAX and TransMIN charged-particle and $p_T^{\text{sum}}$ densities at $\sqrt{s} = 0.3, 0.9, 1.96,$ and 7 TeV. In addition to varying the MPI energy-dependence parameters (Table 1), we also vary the core-matter fraction PARP(83), which parametrizes the amount of matter contained within the radius of the proton core, the CR strength PARP(78), and the CR suppression PARP(77). The PARP(78) parameter reflects the probability for a given string to retain its color history, and therefore does not change the color and other string pieces, while the PARP(77) parameter introduces a $p_T$ dependence on the CR probability [1].

Inelastic events (ND+DD+SD+CD) are generated with PYTHIA6. The best-fit values of the five parameters are shown in Table 4. The matter-core fraction is quite different in the two new PYTHIA6 tunes. This is due to the fact that this parameter is very sensitive to the behaviour of the PDF at small $x$. Predictions obtained with PYTHIA6 Tune Z2*lep, CUETP6S1-CTEQ6L1 and CUETP6S1-HERAPDF1.5LO are compared in Appendix B to the UE data. The new PYTHIA6 tunes significantly improve the description of the UE data relative to PYTHIA6 Tune Z2*lep at all considered
energies, due to the better choice of parameters governing the MPI energy dependence.

2.3 The HERWIG++ UE tunes

Starting with the parameters of HERWIG++ Tune UE-EE-5C [30], we construct a new HERWIG++ UE tune, CUETHppS1, where hpp stands for HERWIG++. This tune is obtained by varying the four parameters shown in Table 5 in the fit to TransMAX and TransMIN charged-particle and $p_T^{\text{sum}}$ densities at the four $\sqrt{s} = 0.3, 0.9, 1.96,$ and $7 \text{ TeV}$. We set the MPI cutoff $p_T^0$ and the reference energy $\sqrt{s_0}$ to the Tune UE-EE-5C values, and vary the MPI c.m. energy extrapolation parameter in Table 1. We also vary the inverse radius that determines the matter overlap and the range of CR. The CR model in HERWIG++ is defined by two parameters, one (\textcolor{red}{\text{colourDisrupt}}) ruling the color structure of soft interactions ($p_T < p_T^0$), and one (\textcolor{red}{\text{ReconnectionProbability}}) giving the probability of CR without a $p_T$ dependence for color strings. We include all four center-of-mass energies, although at each energy we exclude the first two $p_T^{\text{max}}$ bins. These first bins, e.g. for $p_T^{\text{max}} < 1.5 \text{ GeV}$, are sensitive to single-diffraction dissociation, central-diffraction, and double-diffraction dissociation, but HERWIG++ contains only the ND component.

In Table 5, the parameters of the new CUETHppS1 are listed and compared to those from Tune UE-EE-5C. The parameters of the two tunes are very similar. The $\chi^2/\text{dof}$, also
indicated in Table 5, is found to be ≈0.46, which is smaller than the value obtained for other CMS UE tunes. This is due to the fact that the first two bins as a function of $p_T^{\text{max}}$, which have much smaller statistical uncertainties than the higher-$p_T^{\text{max}}$ bins, are excluded from the fit because they cannot be described by any reasonable fit-values. In Appendix C, predictions obtained with HERWIG++ Tune UE-EE-5C and CUEThpS1 are compared to the UE data. The two tunes are both able to reproduce the UE data at all energies. With the new CUEThpS1 tune, uncertainties can be estimated using the eigentunes (Appendix A).

In conclusion, both HERWIG++ tunes, as well as the new CMS PYTHIA6 UE tunes reproduce the UE data at all four $\sqrt{s}$. The PYTHIA8 UE tunes, however, do not describe well
Fig. 6 CMS data at $\sqrt{s} = 7$ TeV [36] for the normalized distributions of the correlation observables $\Delta S$ (left), and $\Delta^{\text{rel}} p_T$ (right) in the W+diJet channel, compared to MADGRAPH (MG) interfaced to: PYTHIA8 Tune 4C, Tune 4C with no MPI, and the CMS PYTHIA8 DPS partial CDPSTP8S1-Wj (top); and CDPSTP8S1-Wj, and CDPSTP8S2-Wj (bottom). The bottom panels of each plot show the ratios of these tunes to the data, and the green bands around unity represent the total experimental uncertainty.

3 The CMS DPS tunes

Traditionally, $\sigma_{\text{eff}}$ is determined by fitting the DPS-sensitive observables with two templates [32–36] that are often based on distributions obtained from QCD MC models. One template is constructed with no DPS, i.e. just single parton scattering (SPS), while the other represents DPS production. This determines $\sigma_{\text{eff}}$ from the relative amounts of SPS and DPS contributions needed to fit the data. Here we use an alternative method that does not require construction of templates from MC samples. Instead, we fit the DPS-sensitive observables directly and then calculate the resulting $\sigma_{\text{eff}}$ from the model. For example, in PYTHIA8, the value of $\sigma_{\text{eff}}$ is calculated by multiplying the ND cross section by an enhancement or a depletion factor, which expresses the
Table 7 The PYTHIA8 parameters, tuning ranges, Tune 4C values [28] and best-fit values of CDPSTP8S1–4j and CDPSTP8S2–4j, obtained from fits to DPS observables in four-jet production. Also shown are the predicted values of \( \sigma_{\text{eff}} \) at \( \sqrt{s} = 7 \) TeV, and the uncertainties obtained from the eigentunes.

| PYTHIA8 Parameter | Tuning range | Tune 4C | CDPSTP8S1-4j | CDPSTP8S2-4j |
|-------------------|--------------|---------|--------------|--------------|
| PDF               |              |         | CTEQ6L1      | CTEQ6L1      |
| MultipartonInteractions:pT0Ref [GeV] | 1.0–3.0     | 2.085   | 2.085\(^a\)  | 2.125         |
| MultipartonInteractions:ecmPow | 0.0–0.4     | 0.19    | 0.19\(^a\)   | 0.179         |
| MultipartonInteractions:expPow   | 0.4–10.0    | 2.0     | 1.160        | 0.692         |
| ColourReconnection:range        | 0.0–9.0     | 1.5     | 1.5\(^a\)    | 6.526         |
| MultipartonInteractions:ecmRef [GeV] | –           | 1800    | 1800\(^a\)   | 1800\(^a\)   |
| \( \chi^2/\text{dof} \)      | –            | 0.751   | –             | 0.428         |
| Predicted \( \sigma_{\text{eff}} \) (in mb) | –           | 30.3    | 21.3\(^{+1.2}_{-1.6}\) | 19.0\(^{+4.7}_{-3.0}\) |

\(^a\) Fixed at Tune 4C value

Fig. 7 Distributions of the correlation observables \( \Delta S \) (left) and \( \Delta^{\text{rel}} p_T \) (right) measured in four-jet production at \( \sqrt{s} = 7 \) TeV [37] compared to PYTHIA8 Tune 4C, Tune 4C with no MPI, and CDPSTP8S1-4j. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.

dependence of DPS events on the collision impact parameter. As expected, more central collisions have a higher probability of a second hard scattering than peripheral collisions. The enhancement/depletion factors depend on the UE parameters, namely, on the parameters that characterize the matter-overlap function of the two protons, which for \( \text{bProfile} = 3 \) is determined by the exponential parameter \( \text{expPow} \), on the MPI regulator \( p_{T0} \) in Eq. (2), and the range of the CR. PYTHIA8 Tune 4C gives \( \sigma_{\text{eff}} \approx 30.3 \) mb at \( \sqrt{s} = 7 \) TeV.

In Sect. 2, we determined the MPI parameters by fitting UE data. Here we determine the MPI parameters by fitting to observables which involve correlations among produced objects in hadron–hadron collisions that are sensitive to DPS. Two such observables used in the fit, \( \Delta S \) and \( \Delta^{\text{rel}} p_T \), are defined as follows:

\[
\Delta S = \arccos \left( \frac{\vec{p}_T(\text{object}_1) \cdot \vec{p}_T(\text{object}_2)}{|\vec{p}_T(\text{object}_1)| \times |\vec{p}_T(\text{object}_2)|} \right),
\]

\[
\Delta^{\text{rel}} p_T = \frac{|\vec{p}^{\text{jet1}}_T + \vec{p}^{\text{jet2}}_T|}{|\vec{p}^{\text{jet1}}_T| + |\vec{p}^{\text{jet2}}_T|},
\]

where, for W+dijet production, object_1 is the W boson and object_2 is the dijet system. For four-jet production, object_1 is the hard-jet pair and object_2 is the soft-jet pair. For \( \Delta^{\text{rel}} p_T \) in W+dijet production, jet_1 and jet_2 are the two jets of the dijet system, while in four-jet production, jet_1 and jet_2 refer to the two softer jets.

The PYTHIA8 UE parameters are fitted to the DPS-sensitive observables measured by CMS in W+dijet [36] and in four-jet production [37]. After extracting the MPI parameters, the value of \( \sigma_{\text{eff}} \) in Eq. (3) can be calculated from the underlying MPI model. In PYTHIA8, \( \sigma_{\text{eff}} \) depends primarily on the matter-
Fig. 8  Distributions in the correlation observables $\Delta S$ (top) and $\Delta_{\text{rel}}p_T$ (bottom) measured in four-jet production at $\sqrt{s} = 7$ TeV [37], compared to predictions of PYTHIA8 using CDPSTP8S2-4j and of MADGRAPH (MG) interfaced to PYTHIA8 using CDPSTP8S2-4j (left) and PYTHIA8 using CUETP8M1 and HERWIG++ with CUETHppS1 (right).

Also shown are the ratios of the predictions to the data. Predictions for CUETP8M1 (right) are shown with an error band corresponding to the total uncertainty obtained from the eigentunes (Appendix A). The green bands around unity represent the total experimental uncertainty overlap function and, to a lesser extent, on the value of $p_{T0}$ in Eq. (2), and the range of the CR. We obtain two separate tunes for each channel: in the first one, we vary just the matter-overlap parameter $\text{expPow}$, to which the $\sigma_{\text{eff}}$ value is most sensitive, and in the second one, the whole set of parameters is varied. These two tunes allow to check whether the value of $\sigma_{\text{eff}}$ is stable relative to the choice of parameters.

The W+dijet and the four-jet channels are fitted separately. The fit to DPS-sensitive observables in the W+dijet channel gives a new determination of $\sigma_{\text{eff}}$ which can be compared to the value measured through the template method in the same final state [36]. Fitting the same way to the observables in the four-jet final state provides an estimate of $\sigma_{\text{eff}}$ for this channel.

Table 8 Values of $\sigma_{\text{eff}}$ at $\sqrt{s} = 7$ TeV and 13 TeV for CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, CUETHppS1, and for CDPSTP8S1-4j and CDPSTP8S2-4j. At $\sqrt{s} = 7$ TeV, also shown are the uncertainties in $\sigma_{\text{eff}}$ obtained from the eigentunes.

| CMS tune            | $\sigma_{\text{eff}}$ (mb) at 7 TeV | $\sigma_{\text{eff}}$ (mb) at 13 TeV |
|---------------------|-------------------------------------|-------------------------------------|
| CUETP8S1-CTEQ6L1    | $27.8^{+1.3}_{-1.2}$               | $29.9^{+1.6}_{-1.8}$               |
| CUETP8S1-HERAPDF1.5LO | $29.1^{+2.2}_{-2.0}$               | $31.0^{+3.8}_{-2.6}$               |
| CUETP8M1            | $26.0^{+0.6}_{-0.2}$                | $27.9^{+0.7}_{-0.4}$               |
| CUETHppS1           | $15.2^{+0.5}_{-0.6}$                | $15.2^{+0.5}_{-0.6}$               |
| CDPSTP8S1-4j        | $21.3^{+1.2}_{-1.6}$                | $21.8^{+1.0}_{-0.7}$               |
| CDPSTP8S2-4j        | $19.0^{+4.7}_{-3.0}$                | $22.7^{+10.0}_{-5.2}$              |
3.1 Double-parton scattering in W+dijet production

To study the dependence of the DPS-sensitive observables on MPI parameters, we construct two W+dijet DPS tunes, starting from the parameters of \textsc{pythia8} \textsc{Tune 4C}. In a partial tune only the parameter of the exponential distribution \textsc{expPow} is varied, and in a full tune all four parameters in Table 6 are varied. In a comparison of models with W+dijet events [36], it was shown that higher-order SPS contributions (not present in \textsc{pythia8}) fill a similar region of phase-space as the DPS signal. When such higher-order SPS diagrams are neglected, the measured DPS contribution to the W+dijet channel can be overestimated (i.e. $\sigma_{\text{eff}}$ underestimated). We therefore interface the LO matrix elements (ME) generated by \textsc{MADGRAPH 5} (version 1.5.14) [38] with \textsc{pythia8}, and tune to the normalized distributions of the correlation observables in Eqs. (5) and (6). For this study, we produce \textsc{MADGRAPH} parton-level events with a W boson and up to four partons in the final state. The cross section is calculated using the CTEQ6L1 PDF with a matching scale for ME and parton shower (PS) jets set to 20 GeV. (In Sect. 4, we show that the CMS UE tunes can be interfaced to higher-order ME generators without additional tuning of MPI parameters). Figure 6 shows the CMS data [36] for the observables $\Delta S$ and $\Delta_{\text{rel}}p_T$ measured in W+dijet production, compared to predictions from \textsc{MADGRAPH} interfaced to \textsc{pythia8} Tune 4C, to Tune 4C with no MPI, to the partial CDPSTP8S1-Wj, as well as to the full CDPSTP8S2-Wj (CDPST stands for "CMS DPS

Fig. 9 ATLAS data at $\sqrt{s} = 7$ TeV [39] for charged-particle (left) and $p_T^\text{sum}$ densities (right) with $p_T > 0.5$ GeV and $|\eta| < 2.0$ in the transverse (TransAVE) region compared to predictions of \textsc{pythia8} using CDPSTP8S2-4j (left) and CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, plus \textsc{herwig++} using CUETHppS1 (right). The predictions of CDPSTP8S2-4j are shown with an error band corresponding to the total uncertainty obtained from the eigentunes (Appendix A). The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.
Fig. 10 CMS data on charged-particle (left) and $p_T^{\text{sum}}$ (right) densities at $\sqrt{s} = 0.9$ TeV (top), 2.76 TeV (middle), and 7 TeV (bottom) with $p_T > 0.5$ GeV and $|\eta| < 2.0$ in the transverse (TransAVE) region as defined by the leading charged-particle jet, as a function of the transverse momentum of the leading charged-particle jet. The data are compared to predictions of PYTHIA6 using CUETP6M1-CTEQ6L1, PYTHIA8 using CUETP8M1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, and HERWIG++ using CUETHppS1. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.
Fig. 11 CMS data at $\sqrt{s} = 7$ TeV [17] for particle (top) and $p_T^{\text{miss}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions, as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_{\text{max}}^T$. The data are compared to MADGRAPH (MG), interfaced to PYTHIA8 using CUETP8S1-CTEQ6L1 and CUETP8M1, and to POWHEG (PH), interfaced to PYTHIA8 using CUETP8S1-HERAPDF1.5LO and CUETP8M1. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.

3.2 Double-parton scattering in four-jet production

Starting from the parameters of PYTHIA8 Tune 4C, we construct two different four-jet DPS tunes. As in the W+dijet channel, in the partial tune just the exponential-dependence parameter, expPow, while in the full tune all four parameters of Table 7 are varied. We obtain a good fit to the four-jet data without including higher-order ME contributions. However, we also obtain a good fit when higher-order (real) ME terms are generated with MADGRAPH. In Figs. 7 and 8 the correlation observables $\Delta S$ and $\Delta^\text{rel} p_T$ in four-jet production [37] are compared to predictions obtained with PYTHIA8 Tune 4C, Tune 4C without MPI, CDPSTP8S1-4j, CDPSTP8S2-4j, and MADGRAPH interfaced to CDPSTP8S2-4j. Table 7 gives the best-fit parameters and the resulting $\sigma_{\text{eff}}$ values. The values of $\sigma_{\text{eff}}$ extracted from the CMS PYTHIA8 DPS tunes give the first determination of $\sigma_{\text{eff}}$ in four-jet production at $\sqrt{s} = 7$ TeV. The uncertainties quoted for $\sigma_{\text{eff}}$ are obtained from the eigentunes.
Validation of CMS tunes

Here we discuss the compatibility of the UE and DPS tunes. In addition, we compare the CMS UE tunes with UE data that have not been used in the fits, and we examine how well Drell–Yan and MB observables can be predicted from MC simulations using the UE tunes. We also show that the CMS UE tunes can be interfaced to higher-order ME generators without additional tuning of the MPI parameters.

4.1 Compatibility of UE and DPS tunes

The values of $\sigma_{\text{eff}}$ obtained from simulations applying the CMS PYTHIA8 UE and DPS tunes at $\sqrt{s} = 7\text{ TeV}$ and $\sqrt{s} = 13\text{ TeV}$ are listed in Table 8. The uncertainties, obtained from eigentunes are also quoted in Table 8. At $\sqrt{s} = 7\text{ TeV}$, the CMS DPS tunes give values of $\sigma_{\text{eff}} \approx 20\text{ mb}$, while the CMS PYTHIA8 UE tunes give slightly higher values in the range 26–29 mb as shown in Figs. 8 and 9. Figure 8 shows the CMS DPS-sensitive data for four-jet production at $\sqrt{s} = 7\text{ TeV}$ compared to predictions using CDPSTP8S2-4j, CUETP8M1, and CUETHppS1. Figure 9 shows ATLAS UE data at $\sqrt{s} = 7\text{ TeV}$ [39] compared to predictions obtained with various tunes: CDPSTP8S2-4j with uncertainty bands, CUETP6S1-CTEQ6L1, CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, CUETHppS1, and CUETHppS1. Predictions from PYTHIA8 using CUETP8M1 describe reasonably
Fig. 13 Combined CMS and TOTEM data at $\sqrt{s} = 8$ TeV [50] for the charged-particle distribution $dN_{ch}/d\eta$, in inclusive inelastic (top left), NSD-enhanced (top right), and SD-enhanced (bottom) pp collisions. The data are compared to PYTHIA6 using CUETP6S1-CTEQ6L1, and to PYTHIA8 using CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.

well the DPS observables, but do not fit them as well as predictions using the DPS tunes. On the other hand, predictions using CDPSTP8S2-4j do not fit the UE data as well as the UE tunes do.

As discussed previously, the PYTHIA8 tunes use a single exponential matter-overlap function, while the HERWIG++ tune uses a matter-overlap function that is related to the Fourier transform of the electromagnetic form factor. The CUETHppS1 gives a value of $\sigma_{\text{eff}} \approx 15$ mb, while UE and DPS tunes give higher values of $\sigma_{\text{eff}}$. It should be noted that $\sigma_{\text{eff}}$ is a parton-level observable and its importance is not in the modelled value of $\sigma_{\text{eff}}$, but in what is learned about the transverse proton profile (and its energy evolution), and how well the models describe the DPS-sensitive observables. As can be seen in Fig. 8, predictions using CUETP8M1 describe the DPS-sensitive observables better than CUETHppS1, but not quite as well as the DPS tunes. We performed a simultaneous PYTHIA8 tune that included both the UE data and DPS-sensitive observables, however, the quality of the resulting fit was poor. This confirms the difficulty of describing soft and hard MPI within the current PYTHIA and HERWIG++ frameworks. Recent studies [40,41] suggest the need for introducing parton correlation effects in the MPI framework in order to achieve a consistent description of both the UE and DPS observables.

4.2 Comparisons with other UE measurements

Figure 10 shows charged particle and $p_T^{\text{sum}}$ densities [24,42] at $\sqrt{s} = 0.9$, 2.76, and 7 TeV with $p_T > 0.5$ GeV and $|\eta| <$
2.0 in the TransAVE region, as defined by the leading jet reconstructed by using just the charged particles (also called “leading track-jet”) compared to predictions using the CMS UE tunes. The CMS UE tunes describe quite well the UE measured using the leading charged particle as well as the leading charged-particle jet. Tunes obtained from fits to UE data and combined with higher-order ME calculations \[43\] can also be cross-checked against the data. The CMS UE tunes can be interfaced to higher-order ME generators without spoiling their good description of the UE. In Fig. 11, the charged-particle and $p_T^{\text{sum}}$ densities in the TransMIN and TransMAX regions as a function of $p_T^{\text{max}}$, are compared to predictions obtained with MADGRAPH and POWHEG \[44,45\] interfaced to PYTHIA8 using CUETP8M1-CTEQ6L1 and CUETP8M1. In MADGRAPH, up to four partons are simulated in the final state. The cross section is calculated with the CTEQ6L1 PDF. The ME/PS matching scale is taken to be 10 GeV. The POWHEG predictions are based on next-to-leading-order (NLO) dijet using the CT10nlo PDF \[46\] interfaced to PYTHIA8 based on CUETP8M1, and HERAPDF1.5NLO \[21\] interfaced to the PYTHIA8 using CUETP8S1-HERAPDF1.5LO. The poor agreement below $p_T^{\text{max}} = 5 \text{ GeV}$ in Fig. 11 is not relevant as the minimum $\hat{p}_T$ for MADGRAPH and POWHEG is 5 GeV. The agreement with the UE data in the plateau region of $p_T^{\text{max}} > 5 \text{ GeV}$ is good. All these figures show that CMS UE tunes interfaced to higher-order ME generators do not spoil their good description of the UE data.

4.3 Predicting MB observables

The UE is studied in events containing a hard scatter, whereas most of the MB collisions are softer and can include diffractive scatterings. It is however interesting to see how well predictions based on the CMS UE tunes can describe the properties of MB distributions. Figure 12 shows predictions using CMS UE tunes for the ALICE \[47\] and TOTEM data \[48\] at $\sqrt{s} = 7 \text{ TeV}$ for the charged-particle pseudorapidity distribution, $dN_{\text{ch}}/d\eta$, and for $dE/d\eta$ \[49\] at $\sqrt{s} = 7 \text{ TeV}$.

The pythia8 event generator using the UE tunes describes the MB data better than pythia6 with the UE tune, which is likely due to the improved modelling of single-diffraction dissociation, central-diffraction, and double-diffraction dissociation in pythia8. Predictions with all the UE tunes describe fairly well MB observables in the central region ($|\eta| < 2$), however, only predictions obtained with CUETP8M1 describe the data in the forward region ($|\eta| > 4$). This is due to the PDF used in CUETP8M1. As can be seen in Fig. 14, the NNPDF2.3LO PDF at scales $Q^2 = 10 \text{ GeV}^2$ (corresponding to hard scatterings with $\hat{p}_T \sim 3 \text{ GeV}$) and small $x$, features a larger gluon density than in CTEQ6L1 and HERAPDF1.5LO, thereby contributing to more particles (and more energy) produced in the forward region. We have checked that increasing the gluon distribution in HERAPDF1.5LO at values below $10^{-5}$ improved the description of the charged-particle multiplicity measurements in the forward region.
Fig. 15 CMS data at $\sqrt{s} = 7$ TeV [51] for the inclusive jet cross section as a function of $p_T$ in different rapidity ranges compared to predictions of PYTHIA using CUEP8S1-CTEQ6L1, CUEP8S1-HERAPDF, and CUEP8M1, and of HERWIG++ using CUETHppS1. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.
Fig. 16 CMS data at $\sqrt{s} = 7$ TeV [51] for the inclusive jet cross section as a function of $p_T$ in different rapidity ranges compared to predictions of POWHEG interfaced to PYTHIA8 using CUETP8S1-HERAPDF1.5LO and CUETP8M1. The bottom panels of each plot show the ratios of these predictions to the data, and the green bands around unity represent the total experimental uncertainty.
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Fig. 17 Transverse momentum $p_T$ (left) and rapidity distributions (right) of Z boson production in pp collisions at $\sqrt{s} = 7$ TeV \cite{52}. The data are compared to PYTHIA8 using CUETP8M1, and to POWHEG

4.4 Comparisons with inclusive jet production

In Fig. 15 predictions using CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, and CUETHppS1 are compared to inclusive jet cross section at $\sqrt{s} = 7$ TeV \cite{51} in several rapidity ranges. Predictions using CUETP8M1 describe the data best, however, all the tunes overshoot the jet spectra at small $p_T$. Predictions from the CUETHppS1 underestimate the high $p_T$ region at central rapidity ($|y| < 2.0$). In Fig. 16, the inclusive jet cross sections are compared to predictions from POWHEG interfaced to PYTHIA8 using CUETP8S1-HERAPDF1.5LO and CUETP8M1. A very good description of the measurement is obtained.

4.5 Comparisons with Z boson production

In Fig. 17 the $p_T$ and rapidity distributions of the Z boson in pp collisions at $\sqrt{s} = 7$ TeV \cite{52} are shown and compared to PYTHIA8 using CUETP8M1, and to POWHEG interfaced to PYTHIA8 using CUETP8S1-CTEQ6L1 and CUETP8M1. The prediction using PYTHIA8 with CUETP8M1 (without POWHEG) agrees reasonably well with the distribution of the Z boson at small $p_T$ values. Also, when interfaced to POWHEG, which implements an inclusive Z boson NLO calculation, the agreement is good over the whole spectrum.

In Fig. 18 the charged-particle and $p_T^{\text{sum}}$ densities \cite{26} in the toward, away, and transverse (TransAVE) regions as defined by the Z boson in proton–proton collisions at $\sqrt{s} = 7$ TeV are compared to predictions of PYTHIA8 using CUETP8M1. Also shown are MADGRAPH and POWHEG results interfaced to PYTHIA8 using CUETP8S1-CTEQ6L1 and CUETP8M1. The MADGRAPH generator simulates Drell–Yan events with up to four partons, using the CTEQ6L1 PDF. The matching of ME partons and PS is performed at a scale of 20 GeV. The POWHEG events are obtained using NLO inclusive Drell–Yan production, including up to one additional parton. The POWHEG events are interfaced to PYTHIA8 using CUETP8M1 and CUETP8S1-HERAPDF1.5LO. The predictions based on CUETP8M1 do not fit the Z boson data unless they are interfaced to a higher-order ME generator. In PYTHIA8 only the Born term ($q\bar{q} \rightarrow Z$), corrected for single-parton emission, is generated. This ME configuration agrees well with the observables in the away region in data, when the Z boson recoils against one or more jets. In the transverse and toward regions, larger discrepancies between data and PYTHIA8 predictions appear at high $p_T$, where the occurrence of multijet emission has a large impact. To describe Z boson production at $\sqrt{s} = 7$ TeV in all regions, higher-order contributions (starting with Z+2-jets), as used in interfacing PYTHIA to POWHEG or MADGRAPH, must be included.

5 Extrapolation to 13 TeV

In this section, predictions at $\sqrt{s} = 13$ TeV, based on the new tunes, for observables sensitive to the UE are presented. Figure 19 shows the predictions at 13 TeV for the charged-particle and the $p_T^{\text{sum}}$ densities in the TransMIN, TransMAX, and TransDIF regions, as defined by the leading charged particle as a function of $p_T^{\text{max}}$ based on the five new CMS
Fig. 18 Charged-particle (left) and $p_T^\text{sum}$ densities (right) in the toward (top), away (middle), and transverse (TransAVE) (bottom) regions, as defined by the $Z$-boson direction in Drell–Yan production at $\sqrt{s} = 7$ TeV [26]. The data are compared to PYTHIA8 using CUETP8M1, to MADGRAPH (MG) interfaced to PYTHIA8 using CUETP8S1-CTEQ6L1 and CUETP8M1, and to POWHEG (PH) interfaced to PYTHIA8 using CUETP8S1-HERAPDF1.5LO and CUETP8M1. The green bands in the ratios represent the total experimental uncertainty.
Fig. 19 Predictions at $\sqrt{s} = 13$ TeV for the particle (left) and the $p_T^{\text{sum}}$ densities (right) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (top), TransMAX (middle), and TransDIF (bottom) regions, as defined by the leading charged particle, as a function of the leading charged-particle $p_T^{\text{max}}$ for the five CMS UE tunes: PYTHIA6 CUETP6S1-CTEQ6L1, and PYTHIA8 CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, and HERWIG++ CUETHppS1. Also shown are the ratio of the tunes to predictions of CUETP8S1-CTEQ6L1. Predictions for CUETP8M1 are shown along with the envelope (green bands) of the corresponding eigentunes.
Fig. 20 Charged-particle density at $\sqrt{s} = 7$ TeV for particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (top), TransMAX (middle), and TransDIF (bottom) regions, as defined by the leading charged particle, as a function of the leading charged-particle $p_{\text{max}}^T$. The data are compared to PYTHIA6 using CUETP6S1-CTEQ6L1, to PYTHIA8 using CUETPS81-CTEQ6L1, CUETPS81-HERAPDF1.5LO, and CUETHp8S1, and to HERWIG++ using CUETHppS1. Also shown are the predictions (left) based on the CMS UE tunes at 13 TeV (dashed lines), and the ratio of the 13 TeV to 7 TeV results for the five tunes (right).

UE tunes: CUETP6S1-CTEQ6L1, CUETPS81-CTEQ6L1, CUETPS81-HERAPDF1.5LO, CUETPS8M1, and CUETHppS1. In Fig. 19 the ratio of the predictions using the four CMS tunes to the one using CUETPS8M1 is shown. The predictions at 13 TeV of all these tunes are remarkably similar. It does not seem to matter that the new CMS PYTHIA8 UE tunes do not fit very well to the $\sqrt{s} = 300$ GeV UE data. The new PYTHIA8 tunes give results at 13 TeV similar to the new CMS PYTHIA6 tune and the new CMS HERWIG++ tune. The uncertainties on the predictions based on the eigentunes do not exceed 10 % relative to the central value.

In Figs. 20 and 21 the predictions at $\sqrt{s} = 13$ TeV obtained using the new tunes from 7 TeV are shown for the charged-particle and the $p_T^{\text{sum}}$ densities in the TransMIN, TransMAX, and TransDIF regions, defined as a function of $p_{\text{max}}^T$. Also shown is the ratio of 13 TeV to 7 TeV results for the five tunes. The TransMIN region increases much more rapidly with energy than the TransDIF region. For example, when using CUETPS8M1, the charged-particle and the $p_T^{\text{sum}}$ densities in the TransMIN region for $5.0 < p_{\text{max}}^T < 6.0$ GeV is predicted to increase by 28 and 37 %, respectively, while the TransDIF region is predicted to increase by a factor of two less, i.e. by 13 and 18 % respectively.

In Fig. 22, predictions obtained with PYTHIA8 using CUETPS8S1-CTEQ6L1 and CUETPS8M1, and Tune 4C are compared to the recent CMS data measured at $\sqrt{s} = 13$ TeV [53] on charged-particle multiplicity as a function of pseudorapidity. Predictions from CUETPS8S1-CTEQ6L1...
Fig. 21 Charged $p_{T}^{\text{sum}}$ density at $\sqrt{s} = 7$ TeV for particles with $p_{T} > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (top), TransMAX (middle), and TransDIF (bottom) regions, as defined by the leading charged particle, as a function of the leading charged-particle $p_{T}^{\text{max}}$. The data are compared to PYTHIA6 using CUETP6S1-CTEQ6L1, to PYTHIA8 using CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, and to HERWIG++ using CUETHppS1. Also shown are the predictions (left) based on the CMS UE tunes at 13 TeV (dashed lines), and the ratio of the 13 TeV to 7 TeV results for the five tunes (right).

and CUETP8M1 are shown with the error bands corresponding to the uncertainties obtained from the eigentunes. These two new CMS tunes, although obtained from fits to UE data at 7 TeV, agree well with the MB measurements over the whole pseudorapidity range, while predictions from PYTHIA8 Tune 4C overestimate the data by about 10 %. This confirms that the collision-energy dependence of the CMS UE tunes parameters can be trusted for predictions of MB observables.

### 6 Summary and conclusions

New tunes of the PYTHIA event generator were constructed for different parton distribution functions using various sets of underlying-event (UE) data. By simultaneously fitting UE data at several center-of-mass energies, models for UE have been tested and their parameters constrained. The improvement in the description of UE data provided by the new CMS tunes at different collision energies gives confidence that they can provide reliable predictions at $\sqrt{s} = 13$ TeV, where all the new UE tunes predict similar results for the UE observables.

The observables sensitive to double-parton scattering (DPS) were fitted directly by tuning the MPI parameters. Two W+dijet DPS tunes and two four-jet DPS tunes were constructed to study the dependence of the DPS-sensitive observables on the MPI parameters. The CMS UE tunes perform fairly well in the description of DPS observables, but
they do not fit the DPS data as well as the DPS tunes do. On the other hand, the CMS DPS tunes do not fit the UE data as well as the UE tunes. At present, it is not possible to accurately describe both soft and hard MPI within the current PYTHIA and HERWIG++ frameworks. Fitting DPS-sensitive observables has also provided the DPS effective cross section $\sigma_{\text{eff}}$ associated to each model. This method can be applied to determine the $\sigma_{\text{eff}}$ values associated with different MPI models implemented in the current MC event generators for the production of any final-state with two hard particles.

Predictions of PYTHIA8 using the CMS UE tunes agree fairly well with the MB observables in the central region ($|\eta| < 2$) and can be interfaced to higher-order and multi-leg matrix-element generators, such as POWHEG and MADGRAPH, while maintaining their good description of the UE. It is not necessary to produce separate tunes for these generators. In addition, we have verified that the measured particle pseudorapidity density at 13 TeV is well reproduced by the new CMS UE Tunes. Furthermore, all of the new CMS tunes come with their eigentunes, which can be used to determine the uncertainties associated with the theoretical predictions. These new CMS tunes will play an important role in predicting and analyzing LHC data at 13 and 14 TeV.

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Appendix A: Tables of tune uncertainties

This section provides the values of the parameters corresponding to the eigentunes of the new CMS PYTHIA8 and the HERWIG++ tunes. A change in the $\chi^2$ of the fit that equals the absolute $\chi^2$ value obtained in the tune defines the eigentunes listed in Tables 9, 10, 11 and 12 for the new PYTHIA8 and the new HERWIG++ tunes. The different parameter values indicated refer to the deviation tunes along each of the maximally independent directions in the parameter space, obtained by using the covariance matrix in the region of the best tune. The number of directions defined in the parameter space equals the number of free parameters $n$ used in the fit and results into $2n$ parameter variations, i.e. eigentunes. These variations represent a good set of systematic errors on the given tune.

Table 9  Eigentunes sets for CUETP8S1-CTEQ6L1

| PYTHIA8 parameter                  | 1−  | 1+  | 2−  | 2+  | 3−  | 3+  | 4−  | 4+  |
|------------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| MultipartonInteractions:pT0Ref [GeV] | 2.101 | 2.101 | 2.068 | 2.135 | 2.100 | 2.102 | 2.079 | 2.123 |
| MultipartonInteractions:ecmPow     | 0.191 | 0.231 | 0.210 | 0.211 | 0.231 | 0.191 | 0.191 | 0.231 |
| MultipartonInteractions:expPow     | 1.609 | 1.609 | 1.602 | 1.616 | 1.613 | 1.605 | 1.714 | 1.503 |
| ColourReconnection:range           | 3.030 | 3.609 | 3.313 | 3.313 | 3.311 | 3.314 | 3.314 | 3.311 |

Table 10  Eigentunes sets for CUETP8S1-HERAPDF

| PYTHIA8 parameter                  | 1−  | 1+  | 2−  | 2+  | 3−  | 3+  | 4−  | 4+  |
|------------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| MultipartonInteractions:pT0Ref [GeV] | 2.000 | 2.000 | 1.960 | 2.043 | 1.999 | 2.001 | 1.968 | 2.030 |
| MultipartonInteractions:ecmPow     | 0.275 | 0.226 | 0.250 | 0.250 | 0.226 | 0.275 | 0.274 | 0.227 |
| MultipartonInteractions:expPow     | 1.691 | 1.690 | 1.681 | 1.700 | 1.695 | 1.686 | 1.831 | 1.559 |
| ColourReconnection:range           | 6.224 | 5.972 | 6.096 | 6.096 | 6.101 | 6.091 | 6.091 | 6.101 |

Table 11  Eigentunes sets for CUETP8M1

| PYTHIA8 parameter                  | 1−  | 1+  | 2−  | 2+  |
|------------------------------------|-----|-----|-----|-----|
| MultipartonInteractions:pT0Ref [GeV] | 2.403 | 2.402 | 2.400 | 2.405 |
| MultipartonInteractions:ecmPow     | 0.253 | 0.251 | 0.253 | 0.252 |

Table 12  Eigentunes sets for CUETHppS1

| HERWIG++ parameter                  | 1−  | 1+  | 2−  | 2+  | 3−  | 3+  | 4−  | 4+  |
|------------------------------------|-----|-----|-----|-----|-----|-----|-----|-----|
| MPIHandler:InvRadius               | 2.290 | 2.227 | 2.318 | 2.196 | 2.272 | 2.237 | 2.254 | 2.256 |
| RemnantDecayer:colourDisrupt       | 0.396 | 0.811 | 0.634 | 0.623 | 0.632 | 0.625 | 0.596 | 0.666 |
| MPIHandler:Power                   | 0.396 | 0.351 | 0.331 | 0.408 | 0.399 | 0.342 | 0.361 | 0.381 |
| ColourReconnector:ReconnectionProbability | 0.615 | 0.460 | 0.529 | 0.527 | 0.523 | 0.533 | 0.444 | 0.626 |

Appendix B: Comparisons of PYTHIA6 UE tunes to data

Figures 23, 24, 25 and 26 show the CDF data at $\sqrt{s} = 0.3$, 0.9, and 1.96 TeV, and the CMS data at $\sqrt{s} = 7$ TeV on charged-particle and $p_T^{\text{sum}}$ densities in the TransMIN and TransMAX regions, as a function of the transverse momen-
Fig. 23 CDF data at $\sqrt{s} = 300$ GeV [11] on the particle (top) and $p_T^{\text{sum}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to the PYTHIA6 Tune Z$^*\text{lep}$ and the two new CUETP6S1-CTEQ6L1 and CUETP6S1-HERAPDF1.5LO. The new CMS PYTHIA6 tunes are able to describe the measurements better than Tune Z$^*\text{lep}$, in both the rising and the plateau regions of the spectra.

Appendix C: Comparisons to HERWIG++ UE tunes to data

Figures 27, 28, 29 and 30 show the CDF data at $\sqrt{s} = 0.3$, 0.9, and 1.96 TeV, and the CMS data at $\sqrt{s} = 7$ TeV on the charged-particle and $p_T^{\text{sum}}$ densities in the TransMIN and TransMAX regions as a function of $p_T^{\text{max}}$, and compared with predictions obtained with the HERWIG++ Tune UE-EE-5C and the new CUETHppS1. These two HERWIG++ tunes are very similar and adequately describe the UE data at all four energies.

Appendix D: Additional comparisons at 13 TeV

In this section, a supplementary collection of comparisons among predictions of the new tunes are shown for DPS and MB observables at 13 TeV.
D.1 DPS predictions at 13 TeV

In Fig. 31, the predictions for the DPS-sensitive observables at 13 TeV are shown for the three CMS PYTHIA8 UE tunes: CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, for CUETHppS1, and for the two CMS PYTHIA8 DPS tunes CDPSTP8S1-4j and CDPSTP8S2-4j. In HERWIG++, σ_{eff} is independent of the center-of-mass energy, while PYTHIA8 gives a σ_{eff} that increases with energy. The PYTHIA8 UE tunes predict that σ_{eff} will increase by about 7 % between 7 and 13 TeV, while the CDPSTP8S2-4j predicts an increase of about 20 %. This results in slightly different predictions for the DPS-sensitive observables at 13 TeV for the CMS UE tunes and the CMS DPS tunes.

D.2 MB predictions at 13 TeV

Predictions of the CMS UE tunes at √s = 13 TeV are shown in Fig. 32 for the charged-particle pseudorapidity distribution, dN_{ch}/dη, for inelastic, non single-diffraction-enhanced, and single-diffraction-enhanced proton–proton collisions. In Fig. 32, the ratio of 13 to 8 TeV results is shown for each of the tunes. The densities in the forward region are predicted to increase more rapidly than the central region between 8 and 13 TeV. However, the UE observables in Figs. 20 and 21 increase much faster with center-of-mass energy than do these MB observables.
Fig. 25 CDF data at $\sqrt{s} = 1.96$ TeV [11] on the particle (top) and $p_T^{\text{pim}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to the PYTHIA6 Tune Z2*lep, CUETP6S1-CTEQ6L1 and CUETP6S1-HERAPDF1.5LO. The green bands in the ratios represent the total experimental uncertainties.
Fig. 26 CMS data at $\sqrt{s} = 7\,\text{TeV}$ [17] on the particle (top) and $\rho_{\text{sum}}$ densities (bottom) for charged particles with $p_T > 0.5\,\text{GeV}$ and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to the PYTHIA6 Tune ZA*lep, CUETP6S1-CTEQ6L1 and CUETP6S1-HERAPDF1.5LO. The green bands in the ratios represent the total experimental uncertainties.
Fig. 27 CDF data at $\sqrt{s} = 300$ GeV [11] on particle (top) and $p_T^{\text{sum}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to the HERWIG++ Tune UE-EE-5C and CUETHppS1. The green bands in the ratios represent the total experimental uncertainties.
Fig. 28 CDF data at $\sqrt{s} = 900$ GeV [11] on particle (top) and $p_{T}^{\text{sum}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_T^{\text{max}}$. The data are compared to the HERWIG++ Tune UE-EE-5C and CUETHppS1. The green bands in the ratios represent the total experimental uncertainties.
Fig. 29 CDF data at $\sqrt{s} = 1.96$ TeV [11] on particle (top) and $p_{T}^{\text{ch}}$ densities (bottom) for charged particles with $p_{T} > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged-particle $p_{T}^{\text{max}}$. The data are compared to the HERWIG++ Tune UE-EE-5C and CUETHppS1. The green bands in the ratios represent the total experimental uncertainties.
Fig. 30 CMS data at $\sqrt{s} = 7$ TeV [17] on particle (top) and $p_T^{\text{cm}}$ densities (bottom) for charged particles with $p_T > 0.5$ GeV and $|\eta| < 0.8$ in the TransMIN (left) and TransMAX (right) regions as defined by the leading charged particle, as a function of the transverse momentum of the leading charged particle $p_T^{\text{max}}$. The data are compared to the HERWIG++ Tune UE-EE-SC and CUETHppS1. The green bands in the ratios represent the total experimental uncertainties.
Fig. 31 Predictions at $\sqrt{s} = 13$ TeV for the normalized distributions of the correlation observables $\Delta S$ (left), and $\Delta_{\text{rel}}p_T$ (right) for four-jet production in pp collisions for the three CMS PYTHIA8 UE tunes CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1, for CUETHppS1, and for CDPSTP8S1-4j and CDPSTP8S2-4j. Also shown are the ratios of the tunes to predictions of CUETP8S1-CTEQ6L1.
Fig. 32 Predictions at $\sqrt{s} = 13$ TeV for the charged-particle pseudorapidity distribution $dN_{ch}/d\eta$, for (top) inelastic, (middle) NSD-enhanced, and (bottom) SD-enhanced pp collisions from CUETP6S1-CTEQ6L1, CUETP8S1-CTEQ6L1, CUETP8S1-HERAPDF1.5LO, and CUETP8M1. Also shown are the ratios of the tunes to predictions of CUETP8M1, and the ratio of 13 to 8 TeV results for each of the tunes (right).
42. CMS Collaboration, Measurement of the underlying event activity using charged-particle jets in proton–proton collisions at $\sqrt{s} = 2.76$ TeV. JHEP 09, 137 (2015). doi:10.1007/JHEP09(2015)137. arXiv:1507.07229

43. B. Cooper et al., Importance of a consistent choice of $\alpha_s$ in the matching of AlpGen and Pythia. Eur. Phys. J. C 72, 2078 (2012). doi:10.1140/epjc/s10052-012-2078-y. arXiv:1109.5295

44. P.A. Nason, in Proceedings, 9th International Symposium on Radiative Corrections: Applications of Quantum Field Theory to Phenomenology. (RADCOR 2009), vol. RADCOR2009. Recent developments in POWHEG (2010), p. 018. arXiv:1001.2747

45. S. Alioli, P. Nason, C. Oleari, E. Re, A general framework for implementing NLO calculations in shower Monte Carlo programs: the POWHEG BOX. JHEP 06, 043 (2010). doi:10.1007/JHEP06(2010)043. arXiv:1002.2581

46. H.-L. Lai et al., New parton distributions for collider physics. Phys. Rev. D 82, 074024 (2010). doi:10.1103/PhysRevD.82.074024. arXiv:1007.2241

47. ALICE Collaboration, Charged-particle multiplicity measurement in proton–proton collisions at $\sqrt{s} = 7$ TeV with ALICE at LHC. Eur. Phys. J. C 68, 345 (2010). doi:10.1140/epjc/s10052-010-1350-2. arXiv:1004.3514

48. TOTEM Collaboration, First measurement of the total proton–proton cross section at the LHC energy of $\sqrt{s} = 7$ TeV. Europhys. Lett. 96, 21002 (2011). doi:10.1209/0295-5075/96/21002. arXiv:1110.1395

49. CMS Collaboration, Measurement of energy flow at large pseudorapidities in pp collisions at $\sqrt{s} = 0.9$ and 7 TeV. JHEP 11, 148 (2011). doi:10.1007/JHEP02(2012)055. arXiv:1110.0211

50. CMS and TOTEM Collaborations, Measurement of pseudorapidity distributions of charged particles in proton–proton collisions at $\sqrt{s} = 8$ TeV by the CMS and TOTEM experiments. Eur. Phys. J. C 74, 3053 (2014). doi:10.1140/epjc/s10052-014-3053-6. arXiv:1405.0722

51. CMS Collaboration, Measurement of the inclusive jet cross section in pp collisions at $\sqrt{s} = 7$ TeV. Phys. Rev. Lett. 107, 132001 (2011). doi:10.1103/PhysRevLett.107.132001. arXiv:1106.0208

52. CMS Collaboration, Measurement of the rapidity and transverse momentum distributions of Z bosons in pp collisions at $\sqrt{s} = 7$ TeV. Phys. Rev. D 85, 032002 (2012). doi:10.1103/PhysRevD.85.032002. arXiv:1106.4973

53. CMS Collaboration, Pseudorapidity distribution of charged hadrons in proton–proton collisions at $\sqrt{s} = 13$ TeV. Phys. Lett. B 751, 143 (2015). doi:10.1016/j.physletb.2015.10.004. arXiv:1507.05915

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