Cosmological Implications of Low Energy
Supersymmetry Breaking Models

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Abstract

We show that stable local cosmic strings are a generic prediction of supersymmetric models where supersymmetry is broken at scales within a few orders of magnitude of the weak scale and is fed down to the observable sector by gauge interactions. The typical energy scale of these strings is about $10^2$ TeV. Since in the most general and natural scenario there are two different sources of contributions to ordinary superpartner masses, gauge mediation from the messenger sector and anomalous $U(1)$ $D$-terms, novel features are that the cosmic strings may be superconducting with the role of bosonic charge carriers played by squarks and sleptons and that some baryonic or leptonic charge may be stored in the core of the string. Possible cosmological and astrophysical implications of these superconducting strings are discussed.
1. Supersymmetry (SUSY) provides solutions to solve many of the puzzles of the standard model such as the stability of the weak scale under radiative corrections as well as the origin of the weak scale itself. Local supersymmetry provides a promising way to include gravity within the framework of unified theories of particle physics, eventually leading the way to a theory of everything in string models. For these very good reasons, supersymmetric extensions of the standard model (MSSM) have been the focus of intense theoretical activity in recent years [1]. Since experimental observations require supersymmetry to be broken, it is essential to have a knowledge of the nature and the scale of supersymmetry breaking in order to have a complete understanding of the physical implications of these theories. At the moment, we lack such an understanding and therefore it is important to explore the various ways in which supersymmetry breaking can arise and study their consequences.

There are several hints from the study of general class of MSSM which could perhaps be useful in trying to explore the nature of supersymmetry breaking. Two particular ones that rely on the supersymmetric sector of model are (i) the natural suppression of flavor changing neutral currents (FCNC), which require either a high degree of degeneracy among squarks of different flavor or the first two generations of squarks to be much heavier than the weak scale, and (ii) stringent upper limits on the electric dipole moment of the neutron (EDMN), which imply severe constraints on the gaugino masses as well as on the $A$ and $B$ terms of MSSM [2]. One could take the point of view that these observational facts may be telling us something about the nature of supersymmetry breaking. If this is true, then it is important to isolate those SUSY breaking scenarios which realize the above properties in a simple manner and study their implications.

The most common and popular approach is to implement supersymmetry breaking in some hidden sector where some $F$-term gets a vacuum expectation value (VEV) and then transmit it to the standard model sector by gravitational interactions. This is the so-called hidden $N = 1$ supergravity scenario [1]. If one arranges the parameters in the hidden sector in such a way that the typical $\langle F \rangle$-term is of the order of $\langle F \rangle^{1/2} \sim \sqrt{(1 \text{ TeV})M_{Pl}} \sim 10^{11}$ GeV, where $M_{Pl} = 2.4 \times 10^{18}$ GeV, the gravitino mass $m_{3/2}$ turns out to be of the order of the TeV scale. In the $N = 1$ supergravity scenario, however, the flavor-blindness is likely to be spoiled in the Kähler potential. One possibility is that the underlying theory possesses some flavor symmetry, but these symmetries must be broken and it is hard to reconcile the strong violation of flavor in the fermion sector with the degeneracy in the sfermion sector. The suppression of the EDMN is also hard to explain in supergravity since one expects the
bilinear and trilinear terms to be of the order of $m_{3/2}$ and explicit CP-violating phases to be $O(1)$.

In this paper we will concern ourselves with alternative scenarios where supersymmetry is broken dynamically or via the O’Raifeartaigh mechanism at low energies, within a few orders of magnitude of the weak scale.

Gauge interactions can serve as the messengers of supersymmetry breaking and the SUSY breaking mediators are fields that transform nontrivially under the standard model gauge group. These are the so-called gauge mediated supersymmetry breaking (GMSB) models. The soft SUSY breaking mass terms of sfermions get contributions at two-loop, $\tilde{m}^2 \sim \left(\frac{\alpha}{4\pi}\right)^2 \Lambda^2$, where $\Lambda \sim 10$ TeV is the typical scale of the messenger sector. The GMSB models have the extra advantage that the FCNC effects are naturally suppressed. This is due to the fact that at the scale $\Lambda$ the squark masses are all degenerate because of the flavor blindness of the standard model gauge group. Only a slight asymmetry is introduced by renormalization group extrapolation from the scale $\Lambda$ to low energies. Moreover, the trilinear soft breaking terms $A$ vanish at $\Lambda$ rendering the CP-violation problem milder.

Recently, an alternative approach have been proposed in which gauginos, higgsinos and the third generation of squarks are sufficiently light to stabilize the electroweak scale, but the two first generations of squarks and sleptons are sufficiently heavy to suppress the FCNC and the EDMN below the experimental bound. This class of models is dubbed ”more” minimally supersymmetric than the MSSM since they do not require some ad hoc supposition of degeneracy or alignment. In most of the attempts made so far along this line the crucial feature is the existence of an anomaly-free $U(1)$ gauge group, which appears anomalous below some scale $M$. The effective theory includes a Fayet-Iliopoulos (FI) $D$-term proportional to $\text{Tr} Q M^2$, where the $Q$’s represent the $U(1)$ charges of the heavy fields which have been integrated out.

1 In this paper we will not be concerned with the case in which the $U(1)$ group emerges from string theories and the anomaly is cancelled by the Green-Schwarz mechanism. The FI $D$-term is expected to be of the order of the stringy scale ($10^{17} - 10^{18}$) GeV. Cosmic strings in the framework of anomalous $U(1)$ superstring theories have been discussed in [11] and recently in [12]. The mass of the $U(1)$ gauge field receives contribution from the dilaton VEV $\langle S + \overline{S} \rangle$ and from any other field $\Phi$ which is charged under $U(1)$ and has nonvanishing VEV. Since the dilaton field, contrary to the $\Phi$ field, is not winding at infinity, the gauge flux will be non-integer. This means that strings arising from anomalous $U(1)$ superstring theories are not local, but semiglobal.
sleptons, contrary to the third generation, carry $U(1)$ charges, the required mass hierarchy is obtained.

The suppression of the FCNC and the EDMN are not the only good features a supersymmetric model should possess though. SUSY models can be regarded as realistic only when they are able to reproduce the quantitative features of the fermion spectrum and the CKM matrix. In a unified picture it is desirable that the solution to all these puzzles reside in the same sector of the theory. Recent investigations have focused on the possibility that a Frogatt-Nielsen flavor mechanism \cite{13} is implemented in the messanger sector \cite{7,8}. This means that the messenger sector is also to be a Frogatt-Nielsen sector and that the messenger $U(1)$ symmetry by which the two first generation fermions get large masses is the same Frogatt-Nielsen $U(1)$ for quarks and leptons. Therefore, the most general (and maybe natural) scenario is an hybrid one where there are two different sources of contributions to ordinary superpartner masses, gauge mediation from the messanger sector and anomalous $U(1)$ $D$-terms \cite{7,8,14}.

The cosmological aspects of the class of supersymmetric models in which SUSY breaking takes place at low energies, of the order of $10^3$ TeV or so, has only been partially explored. It has been suggested that viable cold dark matter candidates may be present in the messanger sector \cite{15}. Inflation might occur at late stages of the evolution of the Universe when its energy density is dominated by a vacuum energy density related to the same $F$-term responsible for the spectrum of supersymmetric particles in GMSB models \cite{16,17}.

In this paper we consider the question of whether one might expect the presence of stable cosmic strings in low energy SUSY breaking models. Over the last two decades, cosmic strings have evoked a great deal of interest as possible remnants of a Grand Unified era in the early Universe as well as possible mechanism for structure formation \cite{18}. However, no compelling particle physics model exist that give rise to such defects.

We would like to show that low energy SUSY breaking models are good candidates. This does not come as a surprise because of the rich gauge group structure. The novel feature is that these cosmic strings may be superconducting with the role of bosonic charge carriers played by squarks and sleptons. This means that in the core of the strings not only the electromagnetic gauge group is spontaneously broken, but also the global baryon ($B$) and the lepton ($L$) symmetries are broken.

This kind of superconducting cosmic strings may have important cosmological and astrophysical effects. Since sfermions may carry a baryonic $U(1)$ global charge, a certain amount
of baryonic charge may be present inside the strings. As a consequence, the baryon asymmetry might be generated in some unconventional way. Primordial magnetic fields might be formed by a network of charged-current carrying cosmic strings. Such fields could account for the observed galactic and intergalactic magnetic fields since they might be suffice to seed magnetic dynamos on galactic scales. We will comment about these and other cosmological aspects in the following. Let us first show that cosmic strings are a generic prediction of low energy SUSY breaking models.

2. As is known, stable cosmic strings arise when the manifold \( M \) of degenerate vacua has a non-trivial first homotopy group, \( \Pi_1(M) \neq 1 \). A generic feature of low energy SUSY breaking models is that the gauge group of the secluded sector, where supersymmetry is broken, may be of the form \( G \otimes U(1)_m \). The group \( U(1)_m \) is usually some global \( U(1) \) which is gauged and made anomaly-free. The fields in the messenger sector are charged under \( U(1)_m \) and (some of them) under the standard model gauge group. When supersymmetry is broken in the secluded sector, some scalar fields in this sector may acquire a vacuum expectation value (VEV), but leave the \( U(1)_m \) gauge symmetry unbroken. As a toy model, let us consider the following superpotential in the secluded sector where a gauge \( U(1)_m \) symmetry has been imposed and \( X \) is a gauge singlet

\[
W = \lambda X (\Phi_1 \Phi_1 - m^2) + M_1 \Phi_1 \Phi_2 + M_2 \Phi_2 \Phi_1.
\]

For \( \lambda^2 m^2 < M_1^2, M_2^2 \), the vacuum of this model is such that \( \langle \phi_i \rangle = \langle \bar{\phi}_i \rangle = 0 \ (i = 1, 2) \), where \( \bar{\phi}_i \) and \( \phi_i \) are the scalar components of the superfields \( \Phi_i \) and \( \bar{\Phi}_i \), respectively. Supersymmetry is broken by the O'Raifeartaigh mechanism and \( \langle F_X \rangle = -\lambda^2 m^2 \). The \( U(1) \) gauge group remains unbroken at this level. Because of supersymmetry breaking, a term like \( V = (F_X \bar{\phi}_1 \phi_1 + \text{h.c.}) \) will appear in the potential. It is easy to show that, integrating out the \( \phi_i \) and \( \bar{\phi}_i \) scalar fields, induces a nonvanishing FI \( D \)-term

\[
\xi \sim \frac{F_X^2}{16 \pi^2 (M_1^2 - M_2^2)} \ln \left( \frac{M_2^2}{M_1^2} \right) .
\]

The presence of the anomalous FI \( D \)-term may induce the spontaneous breakdown of the residual \( U(1)_m \) gauge symmetry along some field direction in the messenger sector. In this case local cosmic strings are formed. Indeed, let us make the very general assumption that integrating out the heavy fields belonging to the secluded sector amounts to generate a positive one-loop FI \( D \)-term \( \xi \) and negative two-loop soft SUSY breaking squared masses for (some of) the scalar fields \( \phi_i \) of the messenger sector. These squared masses are generally proportional to the square of the corresponding \( U(1)_m \) charges \( q_i \). The potential will read
\[ V = -\sum_i q_i^2 \tilde{m}^2 |\phi_i|^2 + \sum_i \left| \frac{\partial W}{\partial \phi_i} \right|^2 + \frac{g^2}{2} \left( \sum_i q_i |\phi_i|^2 + \xi \right)^2, \]  

(3)

where \( g \) is the \( U(1)_m \) gauge coupling constant. From the minimization of (3), one can see that among the fields with \( F \)-flat directions, the one with the smallest negative charge (call it \( \varphi \)) will get a VEV

\[ \langle |\varphi|^2 \rangle = \frac{1}{q_\varphi} \left( \tilde{m}^2 - \frac{g^2}{g^2} \xi \right). \]  

(4)

When this happens, the residual global \( U(1)_m \) symmetry gets broken leading to the formation of local strings.

The string mass per-unit-length is given by \( \mu \sim \xi \). Since \( \sqrt{\xi} \) is a few orders of magnitude larger than the weak scale, cosmic strings are not very heavy (at least in comparison with the most commonly discussed Grand Unified strings) and they are expected to play no role in the generation of the temperature anisotropies in the cosmic microwave background. Yet, they may have other cosmological consequences.

If there are extra local or global \( U(1) \) symmetries in the messenger sector, they can be also spontaneously broken by the FI anomalous \( D \)-term. This happens necessarily if there are no singlet fields charged under the anomalous gauge \( U(1)_m \) only. In such a case, besides the previously mentioned cosmic strings, there may arise cosmic strings associated to the breaking of extra \( U(1) \) factors. However, the condition to produce cosmic strings is \( \Pi_1(\mathcal{M}) \neq 1 \) and one must consider the structure of the whole potential, \( i.e. \) all the \( F \)-terms and all the \( D \)-terms. When this is done, it turns out that, depending on the specific models, some (or all) of the global and local cosmic strings may disappear. In general, there can be models that have just global strings, just local strings, or both global and local strings. Thus, the analysis must be done case by case, but it is important to remember that the class of models predicting global strings are astrophysically ruled out. Indeed, the Goldstone particles associated to the spontaneous breakdown of the global \( U(1) \) are expected to have interactions with the ordinary matter suppressed by the same mass scale of the global cosmic string. Being \( \sqrt{\xi} \) only a few orders of magnitude larger than the weak scale, these Goldstone particles would be copiously emitted from supernovae and stars at an unacceptable level \[[10] \]. This, in particular, may exclude those models in which the

\[ 2 \text{This particular field cannot be charged under the standard model gauge group, but may play the role of the Frogatt-Nielsen field to generate appropriate fermion mass matrices} \[8,14]. \]
secluded and the messenger sectors communicate only through the gauged $U(1)_m$ interaction and no renormalizable couplings among the superfields of the two sectors appear in the superpotential because of the charge assignment. When some scalar fields in the secluded sector acquire a vacuum expectation value the $U(1)_m$ gauge symmetry may be spontaneously broken leaving a residual global $U(1)$ in the messenger sector. This residual global $U(1)$ may be spontaneously broken by the FI $D$-term giving rise to global cosmic strings and astrophysically harmful massless Goldstone modes.

3. Let us now show that the cosmic strings produced in the low energy SUSY breaking models are used to be superconducting. Coming back to the potential \((3)\), we suppose that the quark and/or the lepton superfields are charged under the $U(1)_m$ group. As we argued, this is in the spirit of the "more" MSSM \[3\] and somehow welcome when trying to quantitatively predict the fermion mass spectrum and the CKM matrix.

One could consider a flavor-dependent charge assignment; what it is crucial is to equally charge the first and the second family of down-quarks to be consistent with flavor-violating constraints. The charge assignment for the Higgs superfields $H_U$ and $H_D$ is also model dependent; in order to have the top Yukawa coupling unsuppressed, one has usually to require that the up-type Higgs and the left-handed and right-handed top superfields do not carry any $U(1)_m$-charge. If this is the case, the contribution to the soft supersymmetry breaking mass terms of the stop sector originate from gauge interactions with the messenger fields. If the down-type Higgs superfield carries a charge, $\tan \beta = \langle H_u^0 \rangle / \langle H_d^0 \rangle \gg 1$ is a generic prediction \[7,8\].

Let us focus of one of the sfermion fields\[3\] $\tilde{f}$ with $U(1)_m$-charge $q_f$ such that $\text{sign } q_f = \text{sign } q_{\varphi}$. The potential for the fields $\varphi$ and $\tilde{f}$ is written as

\[
V(\tilde{f}, \varphi) = -q_{\varphi}^2 \tilde{m}^2 |\varphi|^2 - q_f^2 \tilde{m}^2 |\tilde{f}|^2 + \frac{g^2}{2} \left( q_{\varphi} |\varphi|^2 + q_f |\tilde{f}|^2 + \xi \right)^2 + \lambda |\tilde{f}|^4, \tag{5}
\]

where we have assumed, for simplicity, that $\tilde{f}$ is $F$-flat. The parameter $\lambda$ is generated from the standard model gauge group $D$-terms and is vanishing if we take $\tilde{f}$ to denote a family of fields parametrizing a $D$-flat direction.

At the global minimum $\langle \tilde{f} \rangle = 0$ and the electric charge, the baryon and/or the lepton

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\[3\] The role of charge carriers might be played as well by some scalar fields which are charged under the standard model gauge group and are part of the messenger sector. These fields have zero VEV in the true vacuum and are responsible for gauge mediation.
numbers are conserved. The soft breaking mass term for the sfermion reads
\[ \Delta m_f^2 = q_f (q_\phi - q_\bar f) \tilde m^2, \]
which is positive in virtue of the hierarchy \( q_\phi < q_f < 0 \). Consistency with experimental bound requires \( \Delta m_f^2 \) to be of the order of \((20 \text{ TeV})^2\) or so, which in turn requires \( \xi \sim (4\pi/g^2)\tilde m^2 \sim (10^2 \text{ TeV})^2 \). Notice that \( \Delta m_f^2 \) does not depend upon \( \xi \).

Let us analyse what happens in the core of the string. In this region of space, the vacuum expectation value of the field vanishes, \( \langle |\phi| \rangle = 0 \), and nonzero values of \( \langle |\bar f| \rangle \) are energetically preferred in the string core
\[ \langle |\bar f|^2 \rangle = \frac{\tilde m^2 q_f^2 - g^2 \xi q_f}{g^2 q_f^2 + 2\lambda}. \]

Since the vortex is cylindrically symmetric around the z-axis, the condensate will be of the form \( \bar f = \bar f_0(r, \theta) e^{i\eta f(z,t)} \) where \( r \) and \( \theta \) are the polar coordinate in the \((x, y)\)-plane.

The above analysis is not sufficient to show the existence of bosonic charge carriers. One must check that the kinetic term for \( \bar f \) also allows a nonzero value of \( \bar f \) in the string. Following ref. [21] we prove that by showing that the equation of motion for \( \bar f \), linearized around \( \bar f = 0 \), admits growing solutions. This will then show that in the background of the string \( \bar f \) is unstable to the formation of a nonzero condensate on the string. Let us consider the equation of motion of \( \bar f \)
\[ - \partial_\mu \left( \partial^\mu \bar f - ig q_f R^\mu \bar f \right) = \frac{\partial V(\phi, \bar f)}{\partial \bar f} - g^2 q_f^2 R_\mu R^\mu \bar f, \]
where \( R_\mu \) is the \( U(1)_m \) gauge field which takes the form of the Nielsen-Olesen configuration [22]. We may now linearize Eq. (8) around \( \bar f = 0 \) and take the following form for the perturbation of \( \bar f \): \( \delta \bar f = \exp (-i\omega t) g(r) \). The linearized equation of motion reads
\[ - \nabla^2 g(r) + V(r) g(r) = \omega^2 g(r), \]
where \( \nabla^2 \) is the two-dimensional Laplacian and \( V(r) \) represents an "effective" potential. At \( r = 0 \) \( V = -q_f^2 \tilde m^2 + q_f g^2 \xi < 0 \) and \( V \) increases monotonically with \( r \) until it reaches the asymptotic value \( V(\phi, \bar f) = \tilde m^2 q_\phi \xi - (\tilde m^2 q_\phi^2 / g^2) \). The two-dimensional Schrödinger equation above for \( g(r) \) will admit at least one bound state with \( \omega^2 < 0 \). Thus \( \bar f \) is unstable to forming a condensate on the string.

The electric charge, the baryon/and or the lepton numbers are broken inside the string [23]. If there is a condensate \( \bar f \) in the string, then there will be massless excitations of the
Goldstone boson field $\eta_f$ as well. There are different currents on the string world-sheet. One is conserved topologically; being a periodic variable, $\eta_f$ may have a net winding number $N$ around a loop of string associated to the corresponding topological current. This was shown by Witten [20] to imply the existence of a persistent current. The other currents are the electromagnetic and the baryon and/or lepton currents, which are conserved by the equation of motions (at least at the classical level). They may be associated to the relative charges per unit length along the string. In particular, it is intriguing that some baryonic charge may be stored in the core of the string. Indeed, if the sfermion particles are identified with some squarks $\tilde{q}$ (eventually parametrizing a standard model $D$-flat direction), they carry a $U(1)$ baryonic global charge which is derived from the conserved current

$$J_B^\mu = \frac{i}{2} \sum_q q_B^q \left( \tilde{q}^\dagger \partial^\mu \tilde{q} - \tilde{q} \partial^\mu \tilde{q}^\dagger \right),$$

where $q_B^q$ is the baryonic charge associated to any field $\tilde{q}$. Under the assumption of cylindrical symmetry, the baryonic charge per unit length $Q_B$ along the z-axis will be given by $Q_B = \int d\theta dr r j_B(\theta, r)$ where $j_B$ is the current per unit length along the same axis.

Are the superconducting strings stable? If there is no quantum tunnel transition on the string such that $f$ passes through zero, $N$ is conserved and the string is stable. However, if the current on the string gets larger and larger because of some unspecified mechanism, the probability of quantum jumps increases. This results in a maximum value for the current, $I_{\text{max}} \sim e \sqrt{\xi}/g \sim 10^{10}$ A [20].

4. Here we speculate as to the possible implications of the superconducting strings. As the temperature of the Universe decreases and the latter goes through the phase transition at the critical temperature $T_c \sim \sqrt{\xi}$, some of the string-like configurations that were undergoing thermal fluctuations will freeze out and thus not decay. After the phase transition, topological strings can only occur as closed loops or infinite strings.

Because strings are superconducting, during the transition random currents will be induced on the strings. The net current on the loop of a size $\ell$ is expected to be proportional to $T_c(\ell/\xi_I)^{1/2}$ where $\xi_I \sim T_c^{-1}$ is the correlation length of the random currents. The dynamics of the loops is governed by the tension of the string, frictional forces and Hubble expansion. Initially the frictional forces are very large and so the string motion is highly damped. The friction dominated period lasts until the temperature of the Universe has dropped down to the value $T_\ast \approx (\xi/M_{\text{Pl}})$. Since we are interested in low values of supersymmetry breaking scale, only the friction dominated period of string evolution will be relevant. During this
era loops would tend to collapse under their own tension. However, the effective tension of the string is the sum of the bare tension and the square of the current on the string \[24,25\]. As the loops collapses, the current builds up and the effective tension becomes smaller. In such a situation two possibilities may occur: either the current may become so large that the charge carriers can leave the string, that is, the current can saturate, or the effective action goes to zero and the loop does not collapse any further, forming a vorton. If the first possibility is realized, the loops continue to collapse and eventually disappear. If the second possibility is realized, the loops form static ring configuration that can survive until some quantum tunneling causes the charge to leak. Sfermion excitations may leave the world-sheet if their mass in the core of the string is smaller compared to the energy scale of the underlying vortex, though some angular momentum when both \(N\) and the non-topological charges are present can help stabilizing the string. The decay rate is estimated to be of the order of \(\exp \left[-N \left(g^2/4\pi \right)^{3/2} \right] \) \[25\], so that the bosonic vortices are expected to be long-lived for total winding numbers \(N \gg \left(g^2/4\pi \right)^{-3/2}\).

In both cases, depending on the lifetime of the loops and their decay products, their cosmology may be of great interest, especially if a fixed amount of baryonic charge is stored in the string. The generation of the baryon number might occur in some novel way when vortices finally collapse and disappear. Another conceivable scenario is when two straight superconducting strings come into contact. They will start to align because of the strong magnetic interaction of their currents. If one of the string forms a loop, the other would wind up to this loop and the electric field during this gluing up might be large enough to copiously produce pairs of heavy particles and produce the baryon asymmetry \[26\].

With regard to the issue of baryon asymmetry generation, it is important to recall that the presence of the superconducting string is expected to result in the electroweak symmetry being "restored" in the region surrounding the string\[4\] out to a typical distance of the order of \(r \sim 10^{-5} I \text{ GeV}^{-2} \), where \(I\) is the current along the string \[27\]. This happens because the sfermion excited states on the string carry hypercharge and possibly \(T_3\) charge and the physical origin of the symmetry restoration can be directly traced to the coupling of the \(Z\)-field and the Higgs bosons to the strings.

\[4\]What one really means by symmetry restoration is that the standard model Higgs field configurations may be driven to zero in the core of the strings. The standard model gauge group is usually already broken by the sfermion condensate.
It is interesting to notice that these low energy SUSY breaking local strings will carry $Z$-flux inside their core. Moreover, $W$-condensation may take place in some region close to the string \[27\]. If the current inside the string is large enough, the typical length scale of the region where the Higgs field configurations vanish may be larger than $\sim M_W^{-1}$ and sphaleron type effects might be unsuppressed. In such a case, the baryon and the lepton numbers are violated by quantum effects inside the string, but still the linear combination $B - L$ is conserved. This means that if a superconducting string with a certain amount of lepton number is generated and at some point of its evolution the current $I$ is large enough, it might be accompanied by the generation of some baryonic charge. Sphalerons are not always active in the string though. Indeed, any condensate $\phi_i$ carrying $SU(2)_L$ quantum numbers contribute to the sphaleron energy, $E_{\text{sph}} \propto \sqrt{\sum_i |\phi_i|^2}$. Therefore, if the sfermion condensate in the core of the string is charged under $SU(2)_L$, sphaleron transitions are expected to be suppressed even though the Higgs field configurations vanish in the vortex.

Superconducting strings may also be relevant for the generation of a primordial magnetic field \[28,29\]. Small seed fields may be produced by the network of charged-current carrying strings and subsequently amplified by the dynamo mechanism to generate the magnetic field strength observed in our galaxy and many other spiral galaxies \[30\]. This phenomenon depends upon the importance of equilibration processes during the evolution of the currents \[28\]. Superconducting strings formed at the electroweak scale seem to give rise to magnetic fields smaller than required. However, the typical energy scale of the superconducting strings predicted in the framework of low energy SUSY breaking models is appreciably larger than the weak scale and a viable seed magnetic field for the galactic dynamo could be generated if the equilibration is weak. This and other issues, such as the generation of the baryon asymmetry, are presently under investigation.

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