Fully Understanding Generic Objects: Modeling, Segmentation, and Reconstruction

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Abstract

Inferring 3D structure of a generic object from a 2D image is a long-standing objective of computer vision. Conventional approaches either learn completely from CAD-generated synthetic data, which have difficulty in inference from real images, or generate 2.5D depth image via intrinsic decomposition, which is limited compared to the full 3D reconstruction. One fundamental challenge lies in how to leverage numerous real 2D images without any 3D ground truth. To address this issue, we take an alternative approach with semi-supervised learning. That is, for a 2D image of a generic object, we decompose it into latent representations of category, shape, albedo, lighting and camera projection matrix, decode the representations to segmented 3D shape and albedo respectively, and fuse these components to render an image well approximating the input image. Using a category-adaptive 3D joint occupancy field (JOF), we show that the complete shape and albedo modeling enables us to leverage real 2D images in both modeling and model fitting. The effectiveness of our approach is demonstrated through superior 3D reconstruction from a single image, being either synthetic or real, and shape segmentation. Code is available at http://cvlab.cse.msu.edu/project-fully3dobject.html.

1. Introduction

Understanding 3D structure of objects observed from a single view is a fundamental computer vision problem with applications in robotics, 3D perception [2], and AR/VR. As humans, we are able to effortlessly infer the full 3D shape when monocularly looking at an object. Endowing machines with this ability remains extremely challenging. With rises of deep learning, many have shown human-level accuracy on 2D vision tasks, e.g., detection [3, 4], recognition [54, 55], alignment [72]. One key reason for this success is the abundance of labeled data. Thus, the decent performance can be obtained via supervised learning. Yet, extending this success to supervised learning for 3D inference is far behind due to limited availability of 3D labels.

In this case, researchers focus on using synthetic datasets such as ShapeNet [5] containing textured CAD models. To form image-shape pairs for supervised training, many 2D images can be rendered from CAD models. However, using synthetic data alone has two drawbacks. Firstly, making 3D object instances is labor intensive and requires computer graphics expertise, thus not scalable for all object categories. Secondly, the performance of a synthetic-data-trained model often drops on real imagery, due to the obvious domain gap. In light of this, self-supervised methods can be promising to explore, considering the readily available real-world 2D images for any object categories, e.g., ImageNet [44]. If those images can be effectively used in either 3D object modeling or model fitting, it can have a great impact on 3D object reconstruction.

Early attempts [28, 59] on 3D modeling from 2D images in a self-supervised fashion are limited on exploiting 2D images. Given an image, they mainly learn 3D models to re-
construct 2D silhouette [20, 28]. For better modeling, multiple views of the same object with ground-truth pose [36] or keypoint annotations [18] are needed. Recent works [30,35] achieve compelling results by learning from 2D texture cues via a differentiable rendering. However, those methods ignore additional monocular cues, e.g., shading, that contain rich 3D surface normal information. One common issue in prior works is the lack of separated modeling for albedo and lighting, key elements in real-world image formulation. Hence, this would burden the texture modeling for images with diverse illumination variations.

On the other hand, early work on 3D modeling for generic objects [1, 18, 19, 57] often build category-specific models, where each models intra-class deformation of one category. With rapid progress on shape representation, researchers start developing a single universal model for multiple categories. Although such settings expand the scale of training data, it’s challenging to simultaneously capture both intra-class and inter-class shape deformations.

We address these challenges by introducing a novel paradigm to jointly learn a completed 3D model, consisting of 3D shape and albedo, as well as a model fitting module to estimate the category, shape, albedo, lighting and camera projection parameters from 2D images of multiple categories (see Fig. 1). Modeling albedo, along with estimating the environment lighting condition, enables us to compare the rendered image to the input image in a self-supervised manner. Thus, unlabeled real-world images can be effectively used in either 3D object modeling or learning to fit the model. As a result, it could substantially impact the 3D object reconstruction from real data. Moreover, our shape and albedo learning is conditioned on the category, which relaxes the burden of 3D modeling for multiple categories. This design also enhances the representation power for seen categories and generalizability for unseen categories.

A key component in such a learning-based process is a representation effectively representing both 3D shape and albedo for diverse object categories. Specifically, we propose a category-adaptive 3D joint occupancy field (JOF) conditioned on a category code, to represent 3D shape and albedo for multiple categories. Using occupancy field as the shape representation, we can express a large variety of 3D geometry without being tied to a specific topology. Extending to albedo, the color field gives the RGB value of the 3D point’s albedo. Modeling albedo instead of texture opens possibility for analysis-by-synthesis approaches, and exploits shading for 3D reconstruction. Moreover, due to the lack of consistency in meshes’ topology, the dense correspondence between 3D shapes is missing. We propose to jointly model the object part segmentation which exploits its implicit correlation with shape and albedo, creating explicit constraints for our model fitting learning.

In summary, the contributions of this work include:

Table 1. Comparison of 3D object modeling and reconstruction methods. [Keys: CS = category-specific models, SU = a single universal model, Cam = camera parameters, Real data= whether can fine-tune on real-world images self-supervisedly]

| Method       | Model type | Required Cam | Outputs beyond 3D shapes | Real data |
|--------------|------------|--------------|---------------------------|-----------|
| D-R
| SU | X | X | X | X |
| PSG [19] | SU | X | X | X | X |
| AtlasNet [15] | SU | X | X | X | X |
| Pixel2Mesh [60] | SU | X | X | X | X |
| DeepSL [17] | SU | X | X | X | X |
| ONet [13] | CS | X | X | X | X |
| IM-SVR [17] | CS | X | X | X | X |
| Texture Field [56] | CS | X | X | X | X |
| PFNet [45] | CS | X | X | X | X |
| SRN [49] | CS | X | X | X | X |
| NeRF [14] | CS | X | X | X | X |
| MarrNet [74] | CS | X | X | X | X |
| ShapeHD [63] | SU | X | X | X | X |
| F2V [67] | SU | X | X | X | X |
| DRC [55] | CS | X | X | X | X |
| DIST [30] | SU | X | X | X | X |
| Niemeyer et al. [10] | SU | X | X | X | X |
| ESDF [52,55] | CS | X | X | X | X |
| CMR [14,18] | CS | X | X | X | X |
| UMR [25] | CS | X | X | X | X |
| Proposed | SU | X | Albedo | X | X |

- Building a single model for multiple generic objects. The model fully models segmented 3D shape and albedo by a 3D joint occupancy field.
- Modeling intrinsic components enables us to not only better exploit visual cues, but also, leverage real images for model training in a self-supervised manner.
- Introducing a category code into JOF learning, that can enhance the model’s representation ability.
- Incorporating unsupervised segmentation enables better constraints to fine-tune the shape and pose estimation.
- Demonstrating superior performance on 3D reconstruction of generic objects from a single 2D image.

2. Prior Work

3D Object Representation and Modeling. Prior works on 3D object modeling focus more on modeling geometry, based on either point [27, 41, 42], mesh [13, 15, 61], voxel [9, 62, 71], or implicit field [7, 8, 12, 33, 37, 38, 56], while less on texture representation. Current mesh-based texture modeling assumes a predefined template mesh with known topology, limiting to specific object categories, e.g., faces [11, 51–53] or birds [18]. Recently, several works [34, 36, 45, 49] adopt the implicit function to regress RGB values in 3D space, which predicts a complete surface texture. By representing a scene as an opaque and textured surface, SRN [49] learns continuous shape and texture representations from posed multi-view images by a differentiable renderer. Mildenhall et al. [34] represent scenes as neural radiance field allowing novel-view synthesis of more complex scenes. However, as summarized in Tab. 1, all these methods assume known camera parameters or object position, limiting their real-world applicability. Further, they are limited to single categories or scenes. Our universal model
delivers intrinsic 3D decomposition for multiple object categories, which map an image to full 3D shape, albedo, lighting and projection, closing the gap between intrinsic image decomposition and practical applications (Fig. 1).

**Single-view 3D Reconstruction.** Learning-based 3D object modeling [7, 9, 10, 15, 33, 45] can be naturally applied to monocular 3D reconstruction due to its efficient representation. They encode the input image as a latent vector, from which the decoder reconstructs the pose-neutral 3D shape. However, being trained only on synthetic data, many of them suffer from the domain gap. Another direction is to adopt a two-step pipeline [62, 63, 67], to first recover 2.5D sketches, and then infer a full 3D shape. However, despite 2.5D eases domain transfer, they cannot directly exploit 3D cues from images to mitigate uncertainty of 3D representation. A related line of works [17, 29, 30, 35] learn to infer 3D shapes without 3D label by a differentiable render. Another branch of works [14, 18, 22, 23, 25] learn category-specific, deformable models, or canonical surface mappings based on a template from real images. However, one common issue among these works is the lack of albedo and lighting modeling, key elements in image formulation, which limits their ability to fully exploit the 2D image cues.

**3D Shape Co-segmentation.** Co-segmentation operates on a shape collection from a specific category. Prior works [46, 58, 68] develop clustering strategies for meshes, given a handcrafted similarity metric induced by an embedding or graph [16, 48, 65]. Recently, BAE-NET [6] treats shape co-segmentation as occupancy representation learning, with a branched autoencoder. BAE-NET is a joint shape co-segmentation and reconstruction network while cares more on segmentation quality. Our work extends the branched autoencoder to albedo learning. By leveraging correlation between shape and albedo, joint modeling benefits both segmentation and reconstruction.

**3D Morphable Models (3DMMs).** Our framework, as an analysis-by-synthesis approach with 3D shape and albedo models, is a type of 3DMMs [1]. 3DMMs are widely used to model a single object with small intra-class variation, e.g., faces [1], heads [40] or body [31]. 3DMM has not been applied to multiple generic objects due to their large intra-class, inter-class variations and the lack of dense correspondence among 3D shapes [26]. To overcome those limitations, we propose a novel 3D JOF representation to jointly learn a single universal model for multiple generic objects, consisting of both shape and albedo. Together with a model fitting module, it allows semi-supervised training intrinsic 3D decomposition network on unlabeled images.

3. Proposed Method

3.1. Problem Formulation

In this work, a generic object is described by three disentangled latent parameters: category, shape and albedo. Through two deep networks, these parameters can be decoded into the 3D shape and albedo respectively. To have an end-to-end trainable framework, we estimate these parameters along with the lighting and camera projection, via an encoder network, i.e., the fitting module of our model. Three networks work jointly for the objective of reconstructing the input image of generic objects, by incorporating a physics-based rendering layer, as in Fig. 2.

Formally, given a training set of \( T \) images \( \{I_i\}_{i=1}^T \) of multiple categories, our objective is to learn i) an encoder \( \mathcal{E}: I \rightarrow P, L, f_C, f_S, f_A \) that outputs the projection \( P \), lighting parameter \( L \), category code \( f_C \in \mathbb{R}^{l_C} \), shape code \( f_S \in \mathbb{R}^{l_S} \), and albedo code \( f_A \in \mathbb{R}^{l_A} \), ii) a shape decoder \( \mathcal{D}_S \) that decodes parameters to a 3D geometry \( S \), represented by an occupancy field, and iii) an albedo decoder \( \mathcal{D}_A \) that decodes parameters into a color field \( A \), with the goal that the reconstructed image by these components \( (P, L, S, A) \) can well approximate the input. This objective can be mathematically presented as:

\[
\arg\min_{\mathcal{E}, \mathcal{D}_S, \mathcal{D}_A} \sum_{i=1}^T \| \hat{I}_i - I_i \|_1 ,
\]

where \( \hat{I} = \mathcal{R}(P, L, \mathcal{D}_S(f_C, f_S), \mathcal{D}_A(f_C, f_S, f_A)) \) is the re-
constructed image, and $\mathcal{R}(\cdot, \cdot, \cdot)$ is the rendering function.

### 3.2. Category-adaptive 3D Joint Occupancy Fields

Unlike 2D, the community has not yet agreed on a 3D representation both memory efficient and inferable from data. Recently, implicit representations gain popularity as their continuous functions offer high-fidelity surface. Motivated by this, we propose a 3D joint occupancy fields (JOF) representation to simultaneously model shape and albedo with unsupervised segmentation, offering part-level correspondence for 3D shapes, as in Fig. 3. JOF has three novel designs over prior implicit representations [6, 7, 33, 36, 37]: 1) we extend the idea of unsupervised segmentation [6] from shape to albedo, 2) we integrate shape segmentation into albedo decoder, guiding segmentation by both geometry and appearance cues, and 3) we condition JOF on the category to model multiple categories.

**Category Code.** Unlike prior implicit representations, we introduce a category code $f_C$ as the additional input to the shape and albedo decoders. In training, $f_C$ is supervised by a cross-entropy loss using the class label of each image. In the context of modeling shape deformation of multiple categories, using $f_C$ enables decoders to focus on modeling 	extit{intra-class} deformations via $f_S$. Further, the $f_C$ embedding may generalize to unseen categories too.

**Shape Component.** As adopted from [7, 33, 37], each shape is represented by a function, implemented as a decoder network, $D_S: \mathbb{R}^{1C} \times \mathbb{R}^{1S} \times \mathbb{R}^3 \rightarrow [0, 1]$, which inputs a 3D location $x$, category code $f_C$, shape codes $f_S$ and outputs its probability of occupancy $\alpha$. One appealing property is that the surface normal can be computed by the spatial derivative $\frac{\partial D_S}{\partial x}$ via back-propagation through the network, which is helpful for subsequent tasks such as rendering.

To offer unsupervised part segmentation, we adopt BAENET [6] as the architecture of $D_S$. It is composed of 3 fully connected layers and the final layer is a branched layer that gives the occupancy value for each of $k$ branches, denoted by $\{ o \}_{i=1}^k$ in Fig. 3 (a). Finally, a max pooling on the branch outputs the result of the final occupancy.

**Albedo Component.** Albedo component assigns each vertex on the 3D surface a RGB albedo. One may use a combination of category and albedo codes to represent a colored shape, \textit{i.e.}, $D_A(f_C, f_A, x)$. However, it puts a redundant burden to $f_A$ to encode the object geometry, \textit{e.g.}, the position of the tire, and body of a car. Hence, we also feed the shape code $f_S$ as an additional input to the albedo decoder, \textit{i.e.}, $D_A: \mathbb{R}^{1C} \times \mathbb{R}^{1S} \times \mathbb{R}^4 \rightarrow \mathbb{R}^3$ (Fig. 3(b)).

Inspired by the design of $D_S$, we propose to estimate the albedo for $k$ branches $\{ c \}_{i=1}^k$. For each $x$, the final albedo is $c_{idx}$, where $idx = \arg \max_i (o_i)$ is the index of segment where $x$ belongs to (Fig. 3(c)). This novel design integrates shape segmentation into albedo learning, benefiting both segmentation and reconstruction (Fig. 4). The key motivation is that, different parts of an object often differ in shape and/or albedo, and thus both shall guide the segmentation.

### 3.3. Physics-based Rendering

To render an image ($W \times H$ pixels) from shape, albedo, as well as light parameters $L$ and projection $P$, we first find a set of $W \times H$ 3D surface points corresponding to the 2D pixel. Then the RGB color of each pixel is computed via a lighting model using lighting $L$ and decoder outputs.

**Camera Model.** We assume a full perspective camera model. Any spatial points $x$ in the world space can be projected to camera space by a multiplication between a $3 \times 4$ full perspective projection matrix $P$ and its homogeneous coordinate: $u = P [x, 1]^T = [u, d \cdot v, d \cdot w, d]^T$, where $d$ is the depth value of image coordinate $(u, v)$. Essentially, $P$ can be extended to a $4 \times 4$ matrix. By an abuse of notation in homogeneous coordinates, relation between 3D points $x$ and its camera space projection $u$ can be written as:

$$u = Px, \quad \text{and} \quad x = P^{-1}u. \quad (2)$$

**Surface Point Detection.** To render a 2D image, for each ray from the camera to the pixel $j = (u, v)$, we select one “surface point”. Here, a surface point is defined as the first interior point ($D_S(x) > \tau$), or the exterior point with the largest $D_S(x)$ in case the ray doesn’t hit the object. For efficient training, instead of finding exact surface points, we approximate them via Linear or Linear-Binary search. Intuitively, with the distance margin error of $\epsilon$, in Linear search, along each ray we evaluate $D_S(x)$ for all spatial point candidates $x$ with a step size of $\epsilon$. In Linear-Binary search, after the first interior point is found, as $D_S(x)$ is a continuous function, a Binary search can be used to better approximate the surface point. With the same computational budget, Linear-Binary search leads to better approximation of
surface points, hence higher rendering quality. The search algorithm is detailed in the supplementary material (Supp.).

**Image Formation.** We assume purely Lambertian surface reflectance and distant low-frequency illumination. Thus, the incoming radiance can be approximated via Spherical Harmonics (SH) basis functions $H_{k}$ : $\mathbb{R}^{3} \rightarrow \mathbb{R}$, and controlled by coefficients $L = \{\gamma_{b}\}_{b=1}^{B^{2}}$. At the pixel $j$ with corresponding surface point $x_{j}$, the image color is computed as a product of albedo $A_{j}$ and shading $C_{j}$:

$$I_{j} = A_{j} \cdot C_{j} = D_{A}(x_{j}) \cdot \sum_{b=1}^{B^{2}} \gamma_{b} H_{b} \left( \sigma \left( \frac{\delta D_{O}(x_{j})}{\delta x_{j}} \right) \right),$$ (3)

where $n_{j} = \sigma \left( \frac{\delta D_{O}(x_{j})}{\delta x_{j}} \right)$ is the surface normal direction at $x_{j}$, $L_{2}$-normalized by function $\sigma()$. We use $B=3$ SH bands, which leads to $B^{2}=9$ coefficients for each color channel.

### 3.4. Semi-Supervised Model Learning

While our model is designed to learn from real-world images, we benefit from pre-training shape and albedo with CAD models, given inherent ambiguity in inverse tasks. We first describe learning from images self-supervised, and then pre-training from CAD models with supervision.

#### 3.4.1 Self-supervised Joint Modeling and Fitting

Given a set of 2D images without ground truth 3D shapes, we define the loss as ($\lambda$, the weights):

$$\arg \min_{E, D} \mathcal{L}_{3} = \mathcal{L}_{\text{img}} + \lambda_{1} \mathcal{L}_{\text{sil}} + \lambda_{2} \mathcal{L}_{\text{fea-const}} + \lambda_{3} \mathcal{L}_{\text{reg}},$$ (4)

where $\mathcal{L}_{\text{img}}$ is the photometric loss, $\mathcal{L}_{\text{sil}}$ enforces silhouette consistency, $\mathcal{L}_{\text{fea-const}}$ is the local feature consistency loss, and $\mathcal{L}_{\text{reg}}$ includes two regularization terms ($\mathcal{L}_{\text{alb-const}}, \mathcal{L}_{\text{basis}}$).

**Silhouette Loss.** Given the object’s silhouette $M$, obtained by a segmentation method [43], we define the loss as:

$$\mathcal{L}_{\text{sil}} = \frac{1}{W \cdot H} \sum_{j=1}^{W \cdot H} \| D_{S}(E_{C}(I), D_{S}(E_{S}(I), E_{P}(I)^{-1} u_{j}) - o_{j} 1, (5)

where $E_{C}, E_{S}, E_{P}$ are parts of the encoder that estimate $f_{C}, f_{S}$ and $P$ respectively and the three inputs to $D_{S}$ are $f_{C}$, $f_{S}$ and $x_{j}$. With the occupancy field, the occupancy value $o_{j}$ is 0.5 if $M_{j} = 1$, otherwise $o_{j} = 0$. Here, we also analyze how our silhouette loss differs from prior work. If a 3D shape is represented as a mesh, there is no gradient when comparing two binary masks, unless the predicted silhouette is expensively approximated as in Soft rasterizer [28]. If the shape is represented by a voxel, the loss can provide gradient to adjust voxel occupancy predictions, but not the object orientation [59]. Our loss can update both shape occupancy field and camera projection estimation (Eqn. 5).

**Photometric Loss.** To enforce similarity between our reconstruction and input, we use a $L_{1}$ loss on the foreground:

$$\mathcal{L}_{\text{img}} = \frac{1}{|M|} \| (\hat{I} - I) \odot M \|_{1},$$ (6)

where $\odot$ is the element-wise product.

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**Figure 4.** (a) Local feature extraction. For an image $I_{t}$, part segmentation allows selecting and projecting 3D boundary points onto $I_{t}$. Using their 2D locations to sample the first 3 feature maps of the encoder results in the set of local features $F$, whose eigenvector $v_{t}$ is used in $\mathcal{L}_{\text{fea-const}}$. t-SNE plots of $v_{t}$ from 1,000 car images using the models trained without (b) or with (c) $\mathcal{L}_{\text{fea-const}}$. Blue and red are $v_{t}$ of boundary pixels and randomly sampled pixels respectively. While distributions of random pixels remain scattered, $\mathcal{L}_{\text{fea-const}}$ helps boundary pixels to have more similar feature distribution, thus better semantic correspondence across images.

**Local Feature Consistency Loss.** Our decoders unsupervisedly offer part-level correspondence via learnt segmentation (Fig. 3), with which we assume that the boundary pixels of adjacent segments in one image have a similar distribution of appearance as another image of the same category. This assumption leads to a novel loss function (Fig. 4).

For one segmented 3D shape, we first select $q$ boundary points $U_{3D} \in \mathbb{R}^{q \times 3}$ from all pairs of adjacent segments based on branches of $D_{S}$, i.e., a point and its spatial neighbor shall trigger different branches. These 3D points are projected to the image plane $U_{2D} \in \mathbb{R}^{q \times 2}$ via estimated $P$. Similar to [66], we retrieve features from feature maps via the location $U_{2D}$ and form the local features $F \in \mathbb{R}^{q \times 256}$, where 256 is the total feature dimension of 3 layers. Finally, we calculate the largest eigenvector $v$ of the covariance matrix $(F - \mu)^{T}(F - \mu)$ ($\mu$ is the row-wise mean of $F$), which describes the largest feature variation of $q$ points. Despite two images of the same category may differ in colors, we assume there is similarity in their respective major variations. Thus, we define the local feature consistency loss as:

$$\mathcal{L}_{\text{feas-const}} = \frac{1}{|B|} \sum_{(i,j) \in B} \| v_{i} - v_{j} \|_{1},$$ (7)

where $B$ is a training batch of the same category. This loss drives the semantically equivalent boundary pixels across multiple images to be projected from the same 3D boundary adjoining two 3D segments, thus improving pose and shape estimation.

**Regularization Loss.** We define two regularizations:

- **Albedo local constancy:** assuming piecewise-constant albedo [24], we enforce the gradient sparsity in two directions [47]: $\mathcal{L}_{\text{alb-const}} = \sum_{j \in N_{i}} \omega(j, t) \| A_{j} - A_{i} \|_{p}^{2}$, where $N_{i}$ represents pixel $j$’s 4 neighbor pixels. Assuming that pixels with the same chromaticity (i.e., $c_{j} = I_{j} / I_{j}$) are more likely to have the same albedo, we set the weight $\omega(j, t) = e^{-\alpha \| c_{j} - c_{i} \|^{2}}$, where the color is referred of the
input image. We set $\alpha = 15$ and $p = 0.8$ as in [32].

**Batch-wise White Shading:** Similar to [47], to prevent the network from generating arbitrary bright or dark shading, we use a batch-wise white shading constraint: $L_{bws} = \frac{1}{m} \sum_{j=1}^{m} \| C_j^{(r)} - c \|^2_2$, where $C_j^{(r)}$ is a red channel diffuse shading of pixel $j$. $m$ is the total number of foreground pixels in a mini-batch. $c$ is the average shading target, which is set to 1. The same constraint is applied to other channels.

### 3.4.2 Supervised Learning with Synthetic Images

Before self-supervision, we pre-train with CAD models and synthetic data, vital for converging to faithful solutions.

#### Pre-training Shape and Albedo Decoder.

For auto-encoding 3D shape and albedo, we adopt a 3D CNN as encoder $E'$ to extract category, shape and albedo codes $f_C$, $f_S$, $f_A$ from a $64^3 \times 3$ colored voxel. As in Fig. 5, given a dataset of CAD models, a model (with class label $y$) can be represented as a colored 3D occupancy voxel $V$. Equivalently, it can also be represented by $K$ spatial points $x \in \mathbb{R}^3$ and their occupancy $o$, albedo $c$. We define the following loss:

$$\text{arg min}_{D_S, D_A, E'} L_1 = L_S + L_A + L_C,$$

where $L_S = \sum_{j=1}^{K} \| D_S(E_C(V), E_A(V), x_j) - o_j \|^2_2$, $L_A = \sum_{j=1}^{K} \| D_A(E_C(V), E_A(V), x_j) - c_j \|^2_2$, and $L_C$ is cross-entropy loss for class label $y$. Note that training $E'$ is necessary to learn valid distributions of $f_C$, $f_S$, $f_A$, although $E'$ is discarded after this pre-training step.

#### Pre-training Image Encoder.

Given a CAD model, we render multiple images of the same object with different poses and lighting, each forming a triplet of voxel, image and ground truth projection $(V, I, \tilde{P})$. These synthetic data can supervise the pre-training of encoder $E$ by minimizing the $L_2$ below, where the ground truth shape and albedo parameters are obtained by feeding voxel $V$ into $E'$,

$$L_2 = L_{img} + \sum_{X \in (C, S, A)} \lambda_X \| E_X(I) - \tilde{E}_X(V) \|^2_2 + \lambda_P \| E_P(I) - \tilde{P} \|^2_2.$$

### 3.5. Implementation and Discussion

Our training process contains three steps: 1) $D_S$, $D_A$ and $E'$ are pre-trained on colored voxels and corresponding sampled point-value pairs (Eqn. 8); 2) $E$ is pre-trained with synthetic images by minimizing $L_2$; 3) $E$ and $D_A$ are trained using real images (Eqn. 4). We empirically found that, Step 3 training has incremental gain when updating the shape decoder. But it significantly improves the generalization ability of our encoder on fitting model to real images.

#### 3.4.3 Supervised Learning with Real Images

Despite the incremental gain in fitting to real images, training has incremental gain when updating the shape decoder. As in Fig. 6 (d,e), our reconstructions closely match the ground-truth. Quantitatively, we achieve a promising

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**Figure 5.** Colored 3D voxel encoder $E'$ and decoders pre-training.

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| Table 2. Reconstruction comparison between category-specific (CS) and single universal (SU) models on 13 ShapeNet categories. |
|-----------------|-----------------|-----------------|
| Model           | CS              | SU (w/o category code) | SU (w. category code) |
| Average CD ↓    | 0.149           | 0.193              | 0.168               |

Thus, we opt to freeze the shape decoder after Step 1. For more details about the training setting, please refer to *Supp.*

One key enabler of our learning with real images is the differentiable rendering layer. For the rendering function of Eqn. 3, one can compute partial derivatives over $L$, over $P$ since $x = P^{-1}u$, over $f_C$, $f_S$, $f_A$ as they are the inputs of $D_S$, $D_A$, and over the network parameters of $D_S$, $D_A$. However, although the derivative over $x_j$ can be computed, the surface point search process is not differentiable.

### 4. Experimental Results

#### Data

We use the ShapeNet Core v1 [5] for pre-training in Steps 1-2. Following the settings of [9,33,60], we use CAD models of 13 categories and the same training/testing split. While using the same test set, we render training data ourselves, adding lighting and pose variations. We use real images of Pascal 3D+ [64] in Step 3 training. We select 5 categories (plane, car, chair, couch and table) which overlap with 13 categories in synthetic data.

#### Metrics

We adopt standard 3D reconstruction metrics: F-score [21] and Chamfer-L1 Distance (CD). Following [60], we calculate precision and recall by checking the percentage of points in prediction or ground-truth that can find the nearest neighbor from the other within a threshold $\tau$. Following [33], we randomly sample $100k$ points from ground-truth and estimated meshes, to compute CD.

### 4.1. Ablation and Analysis

#### Single vs. Category-specific Models.

We compare two sets of models on ShapeNet data: category-specific (CS) models and single universal (SU) models. CS models specialize for each particular class, which of course has better reconstruction quality (Tab. 2), and may define upper bound performance for SU. Further, we ablate the single universal model with or without category code $f_C$. Clearly, the one with category code performs better, which shows that the category code does relax the burden on decoders and enable the decoders focus on the intra-class shape deformations.

#### Embedding vs. Unseen Categories

Fig. 6 (a,b) shows t-SNEs of $f_S$ and $f_C$ on 13 categories. We observe that $f_C$ is more discriminative, allowing the shape decoder to capture more intra-class deformations. Further, we explore how well our shape decoder can represent the 3D shape of unseen classes. Thus, we randomly select 20 samples from each of 8 unseen ShapeNet categories. With the sampled point-value pairs of each shape, we optimize its $f_C$ and $f_S$ via back-propagation through our trained shape decoder. As in Fig. 6 (d,e), our reconstructions closely match the ground-truth.
Table 3. Effect of loss terms on pose estimation and reconstruction.

|                  | w/o $L_{\text{gi}}$ | w/o $L_{\text{fea-const}}$ | w/o $L_{\text{reg}}$ | Full model |
|------------------|----------------------|-----------------------------|-----------------------|------------|
| Azimuth angle error $\downarrow$ | 17.89°            | 15.31°                      | 13.32°                | 11.96°     |
| Reconstruction (CD) $\downarrow$ | 0.145              | 0.133                       | 0.137                 | 0.113      |

CD on unseen categories compare to that of unseen samples of seen categories: 0.209 vs. 0.135. Additionally, we ablate our decoder with or without category code: 0.209 vs. 0.267, which demonstrates $f_C$ enhances generalizability to unseen categories. We further visualize the estimated $f_C$ together with all training samples in Fig. 6 (c). As we can see, $f_C$ of unseen classes do not overlap with any training categories.

**Effect of Loss Terms.** Using car images of Pascal 3D+, we compare our full model with its partial variants, in term of pose estimation and reconstruction (Tab. 3). As the silhouette provides strong constraints on global shape and pose, without silhouette loss, performance on both metrics are severely impaired. The regularization helps to disentangle shading from albedo, which leads to better surface normal, thus better shape and pose. The local feature consistency loss helps to fine-tune the model fitting, which improves the final pose and shape estimation. Thus all the loss terms in real data training contribute to the final performance.

**Effect of Training on Real Data.** We evaluate 3D reconstructions on images from Pix3D and Pascal 3D+ using models obtained at different training steps. The model fine-tuned on real images (Pro. (real)) has lower Chamfer distances compare to the model learned without real images (Pro.) for every single category (Tab. 6).

### 4.2. Unsupervised Segmentation

As modeling shape, albedo and co-segmentation are closely related tasks [70], joint modeling allows exploiting their correlation. Following the same setting as [6], we evaluate CS models’ co-segmentation and shape representation power on categories of airplane, chair and table. As in Tab. 4, our model achieves a higher segmentation accuracy than BAE-NET [6]. Further, we compare the ability of two models in representing 3D shapes. By feeding a ground-truth voxel from the testing set to the voxel encoder $\hat{E}$ and then shape decoder $D_S$, we evaluate how well the shape-parameter-decoded shape matches the ground-truth CAD model. The higher IoU and lower CD show that we improve both segmentation and representation accuracy. Further, Fig. 7 shows the co-segmentation across 13 categories by our SU model. Meaningful segmentation appears both within a category and across categories. For example, chair seats, plot in green, consistently correspond to sofa seats, table tops, and bodies of airplane, car and watercraft.

### 4.3. Single-view 3D Reconstruction

**Synthetic Images.** We first evaluate 3D reconstruction on synthetic images. We compare with SOTA baselines that leverage various 3D representations: 3D-R2N2 [9] (voxel), Point Set Generation (PSG) [10] (point cloud), Pixel2Mesh [60], AtlasNet [15], Front2Back [67] (mesh), and IM-SVR [7], ONet [33] (implicit field). All baselines train a single model on 13 categories, except IM-SVR which learns 13 models. We report the results of our SU model, trained only on synthetic images, without Step 3.

In general, our model is able to predict 3D shapes that closely resemble the ground truth (Fig. 8 (a)). Our approaches outperform baselines in most categories and achieves the best mean score, in both CD and F-score (Tab. 5). While using the same shape representation as ours, IM-SVR [7] only learns to reconstruct 3D shapes by minimizing the latent representation difference with ground-truth latent codes. By modeling albedo, our model benefits from learning with both supervised and self-supervised (photometric, silhouette) losses. This results in better performance both quantitatively and qualitatively.

**Real Images.** We evaluate 3D reconstruction on two real image databases, Pascal 3D+ [64] and Pix3D [50] (overlapped categories only). We report two results of our method: a model trained with synthetic data only (Pro.)
and a model fine-tuned on real images of Pascal 3D+ \textit{train} subset \textit{without} access to ground truth 3D shapes (Pro. (real)). Baselines include SOTA methods performed well on real images: 3D-R2N2 [9], DRC [59], ShapeHD [63] and DAREC [39]. Among them, DRC and DAREC were trained on real images of Pascal 3D+ as they adopt a differentiable geometric consistency or domain adaptation in training. 3D-R2N2 and ShapeHD cannot be fine-tuned on real images, without albedo modeling and rendering layer.

As in Fig. 8 (b), our model infers reasonable shapes even in challenging contexts. Quantitatively, Tab. 6 shows that both proposed models outperform other methods in Pascal 3D+. The clear performance gap between our two models shows the importance of training on real data.

As Pascal 3D+ only has 10 CAD models per category as ground truth shapes, ground truth labels may be inaccurate. We therefore conduct experiments on Pix3D database with more precise 3D labels. As in Tab. 6, our fine-tuned model has significantly lower CD and the best quality in Fig. 8 (c) comparing to baselines, which indicates our method can leverage real-world images without 3D annotations via self-supervised learning.

### Table 5. Quantitative comparison of 3D reconstruction on synthetic images of ShapeNet. [Key: Best, Second Best]

| Category | 3D-R2N2 [9] | PSG [10] | Pix2Mesh [60] | IM-SVR [7] | ONet [33] | F2B | Pro. | 3D-R2N2 [9] | PSG [10] | Pix2Mesh [60] | IM-SVR [7] | ONet [33] | F2B | Pro. |
|----------|-------------|----------|---------------|--------------|-------------|-----|------|-------------|----------|---------------|--------------|-------------|-----|------|
| Plut| 0.125 | 0.131 | 0.137 | 0.140 | 0.138 | 0.141 | 0.127 | 0.113 | 28.34 | 69.96 | 73.20 | 75.98 | 81.35 | 76.90 | 79.56 |
| car | 0.213 | 0.169 | 0.180 | 0.141 | 0.123 | 0.159 | 0.161 | 0.115 | 37.80 | 50.70 | 67.86 | 66.72 | 75.89 | 68.30 | 75.68 |
| airplane | 0.227 | 0.137 | 0.187 | 0.104 | 0.137 | 0.147 | 0.127 | 0.123 | 41.46 | 68.20 | 71.12 | 70.22 | 79.15 | 77.47 | 74.96 |
| cellphone | 0.195 | 0.161 | 0.149 | 0.128 | 0.131 | 0.140 | 0.135 | 0.130 | 42.31 | 55.95 | 70.24 | 71.97 | 71.27 | 77.15 | 73.91 |
| bench | 0.194 | 0.181 | 0.201 | 0.138 | 0.173 | 0.155 | 0.177 | 0.137 | 34.09 | 49.20 | 57.57 | 65.31 | 65.60 | 66.59 | 66.15 |
| watercraft | 0.238 | 0.188 | 0.212 | 0.151 | 0.157 | 0.218 | 0.171 | 0.143 | 37.10 | 51.28 | 55.12 | 63.70 | 63.15 | 63.04 | 60.90 |
| chair | 0.270 | 0.217 | 0.265 | 0.209 | 0.199 | 0.228 | 0.184 | 0.160 | 40.22 | 41.60 | 54.38 | 57.62 | 62.41 | 64.72 | 63.24 |
| table | 0.239 | 0.222 | 0.218 | 0.190 | 0.173 | 0.189 | 0.167 | 0.172 | 43.79 | 53.44 | 66.30 | 69.49 | 70.33 | 74.80 | 71.27 |
| cabinet | 0.217 | 0.215 | 0.196 | 0.175 | 0.198 | 0.167 | 0.238 | 0.174 | 49.88 | 39.93 | 60.39 | 55.95 | 68.42 | 56.64 | 64.79 |
| couch | 0.229 | 0.224 | 0.212 | 0.177 | 0.194 | 0.194 | 0.209 | 0.186 | 40.01 | 36.59 | 51.90 | 52.61 | 59.93 | 61.59 | 62.01 |
| monitor | 0.314 | 0.284 | 0.239 | 0.198 | 0.225 | 0.278 | 0.185 | 0.208 | 34.38 | 40.53 | 51.39 | 56.55 | 59.42 | 63.03 | 71.45 |
| speaker | 0.318 | 0.316 | 0.285 | 0.245 | 0.252 | 0.300 | 0.227 | 0.245 | 45.30 | 32.61 | 48.84 | 48.63 | 56.87 | 59.10 | 63.19 |
| lamp | 0.778 | 0.314 | 0.308 | 0.385 | 0.362 | 0.479 | 0.209 | 0.276 | 32.35 | 41.40 | 48.15 | 57.42 | 56.18 | 65.11 | 63.38 |
| Mean | 0.278 | 0.188 | 0.216 | 0.175 | 0.187 | 0.215 | 0.173 | 0.168 | 39.01 | 48.58 | 59.72 | 62.75 | 66.92 | 67.26 | 68.49 |

### Table 6. Real 3D reconstruction (CD, \[\frac{\text{cm}}{\text{m}}\]) on Pascal 3D+ and Pix3D.

| Category | 3D-R2N2 [9] | DRC [59] | ShapeHD [63] | DAREC [39] | Pro. | Pro. (real) |
|----------|-------------|----------|---------------|-------------|------|------------|
| plane | 0.035 | 0.172 | 0.094 | 0.108 | 0.114 | 0.102 |
| car | 0.205 | 0.099 | 0.129 | 0.100 | 0.128 | 0.113 |
| chair | 0.238 | 0.158 | 0.137 | 0.135 | 0.138 | 0.119 |
| table | 0.321 | 0.162 | 0.153 | - | 0.167 | 0.127 |
| couch | 0.347 | 0.169 | 0.176 | - | 0.157 | 0.138 |
| Mean | 0.363 | 0.140 | 0.138 | - | 0.141 | 0.120 |
| couch | 0.239 | 0.160 | 0.123 | 0.112 | 0.182 | 0.091 |
| table | 0.307 | 0.178 | 0.137 | - | 0.142 | 0.114 |
| Pix3D | 0.289 | 0.163 | 0.133 | - | 0.145 | 0.127 |
| Mean | 0.278 | 0.167 | 0.131 | - | 0.137 | 0.111 |

### 5. Conclusions

To better leverage real-world images in 3D modeling, we present a semi-supervised learning approach jointly learns the models and the fitting algorithm. While there still be a need of CAD models, our framework, with carefully-designed representation, architectures and loss functions, are able to effectively exploit real images in the training without 3D ground truth. Essentially, our method is applicable to any object category if both i) in-the-wild 2D images and ii) CAD models are available. We are interested in applying our method to a wide variety of object categories.
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