Rationally reduced libraries for combinatorial pathway optimization minimizing experimental effort

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Rational flux design in metabolic engineering approaches remains difficult since important pathway information is frequently not available. Therefore empirical methods are applied that randomly change absolute and relative pathway enzyme levels and subsequently screen for variants with improved performance. However, screening is often limited on the analytical side, generating a strong incentive to construct small but smart libraries. Here we introduce RedLibs (Reduced Libraries), an algorithm that allows for the rational design of smart combinatorial libraries for pathway optimization thereby minimizing the use of experimental resources. We demonstrate the utility of RedLibs for the design of ribosome-binding site libraries by in silico and in vivo screening with fluorescent proteins and perform a simple two-step optimization of the product selectivity in the branched multistep pathway for violacein biosynthesis, indicating a general applicability for the algorithm and the proposed heuristics. We expect that RedLibs will substantially simplify the refactoring of synthetic metabolic pathways.
Synthetic biology is the forward engineering of biological systems, a process in which well characterized, predefined parts are combined in a rational manner to create a desired behaviour or function. However, even well characterized parts can create unpredictable behaviour when introduced into new contexts, for instance when a recombinant pathway causes metabolic imbalances, thus leading to impaired growth and reduced product yields. A possible reason for this dilemma are regulatory mechanisms that ensure optimal balance of a pathway in its natural context but are absent or non-functional in the new host. In fact, recombinant pathways are frequently only poorly understood and important information is missing such as the specific activity of enzymes, intermediate toxicity and/or sinks and occurrence of branching points in the pathway, to name but a few. Consequently, enzyme levels have to be optimized to improve the desired properties.

This lack of knowledge prohibits strictly rational design methods, which are replaced by the creation of diversity and subsequent screening/selection, a process known as directed evolution. This can lead to the emergence of significantly enhanced functions as demonstrated in a number of compelling cases, and consequently be employed to identify optimal absolute and relative abundance of all enzymes constituting a pathway or the ‘metabolic sweet spot’ within a complex expression level space of dimensionality \( m \) (number of proteins) and resolution \( n \) (expression levels tested per protein, Fig. 1). To alter and fine-tune expression levels several methods have been developed: targeting gene dosage, transcriptional regulation, codon usage, and protein half-life.

A promising alternative is the tailoring of translation rates by engineering the ribosomal-binding site (RBS). RBS tailoring is applicable for a wide range of different hosts and has been exploited by recruiting a set of experimentally pre-characterized RBSs for combinatorial optimization of expression levels. However, the effective RBS strength varies strongly for different genes due to differences in its natural context but are absent or non-functional in the new host. Regulatory mechanisms that ensure optimal balance of a pathway remain inevitable. Therefore, smart libraries need to be generated for experimental implementation by easy one-pot cloning procedures.

Finding globally optimal degenerate sequences is not a trivial problem since the number of degenerate sequences to be analysed scales even faster with the number of randomized bases than the aforementioned combinatorial explosion due to the 15-letter IUPAC base code of explicit and degenerate bases. A biophysical model was developed which calculates approximate rates for translation initiation (TIRs), the rate limiting step in translation, strictly based on the RBS sequence facilitating the rational prediction of relative expression levels and the forward design of RBSs (see elsewhere for a review about available algorithms). However, direct application of RBS prediction for refactoring of pathways is difficult since optimal expression levels are unknown and the predictive models are only approximate and do not include important factors such as gene dosage and promoter activity. This suggests that the exploration of a range of different TIRs rather than a specific value is the most advantageous strategy and combinatorial optimization to identify the metabolic sweet spot remains inevitable. Therefore, smart libraries need to be generated that (i) cover a broad range of expression levels; (ii) are uniformly distributed; (iii) have a size that is amenable to screening; and (iv) are encoded by single degenerate sequences, which allow for experimental implementation by easy one-pot cloning procedures.

Figure 1 | Multidimensional expression level optimization. To optimize the flux within a pathway composed of \( m \) enzymatic steps the expression level of each component has to be randomized concomitantly (e.g., by RBS engineering) to identify the metabolic sweet spot in a space that is otherwise dominated by regions of undesired behaviour including low product titers, accumulation of intermediates, or metabolic burden. The number of different expression levels \( n \) per pathway component determines the resolution of the search leading to a problem of quickly rising complexity for higher numbers of pathway components \( m \) and higher resolution \( n \). The complexity of the search (i.e., the number of possible expression level combinations) can be calculated according to \( r^m \).

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\text{Complexity} = r^m
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effort and generation of libraries that cover large ranges of TIRs, but does not deliver a global optimum and still retains a skew towards low-level TIRs due to the exponential binning.

Here we introduce the algorithm RedLibs (Reduced Libraries) that identifies globally optimal degenerate RBSs that uniformly span the entire TIR space in a linear manner. RedLibs compares the TIR distributions of all possible degenerate RBSs to a desired target distribution, leading to truly uniform predicted distributions that can be implemented by simple one-pot cloning protocols. We characterize these libraries by in silico and in vivo screening for two fluorescent proteins in different library sizes. Next, we demonstrate the applicability of RedLibs to a common metabolic engineering problem, the flux optimization around a branching point in a pathway, here for violacin biosynthesis. This example is representative for common low-throughput analysis methods and the pathway products are highly relevant because of their medical properties.

Finally, we exploit the high density of functional clones in RedLibs-derived libraries to develop a novel iterative method that allows for the identification a metabolic sweet spot with highly reduced analytical effort.

**Results**

**Algorithm for rational reduction of library size.** We developed RedLibs (freely available at: https://www.bse.uzh.ch/bpl/software/redlibs), an algorithm that produces a partially degenerate RBS sequence coding for a library that allows for the most uniform sampling of the entire accessible translation level space for a target protein while concomitantly keeping the library at a small, user-specified size (Fig. 2). The algorithm requires a gen- and context-specific input data set of sequence TIR pairs generated by RBS prediction software like the RBS calculator. For example, one can generate prediction data for a fully degenerate SD sequence (e.g., eight consecutive Ns) in front of the gene for the red fluorescent protein mCherry and receive a list of $4^8 = 65,536$ RBS sequences with their corresponding predicted TIRs. As discussed, this initial RBS library is not well suited for implementation as it is too large and highly redundant for RBSs, which will lead to poor translation (e.g., for mCherry > 99.5% of the library members exhibit a TIR of < 10% of the entire range) (Fig. 2a). RedLibs uses this skewed input data set to produce smart sub-libraries of a user-specified target size that match the desired distribution (e.g., uniform distribution) as closely as possible and are encoded by a single degenerate sequence suitable for the cloning of a one-pot library.

These sub-libraries are generated by computing the TIR distributions of all possible partially degenerate sequences with a given target size (these sequences are obtained from a database which is part of RedLibs) and subsequently comparing them to the target distribution one by one. More precisely, this comparison is carried out by calculating the cumulative distribution function (CDF) for each sub-library and matching it with the CDF of the predefined target distribution (e.g., uniform over the entire TIR space). The largest deviation between both CDFs, the Kolmogorov–Smirnov distance $d_{KS}$, represents a quantitative measure of resemblance between the distributions. Sequences with a low $d_{KS}$ are more similar to the target distribution than those with a large $d_{KS}$ (Fig. 2b). Finally, the distributions are ranked according to $d_{KS}$ and the ranked list is returned to the user. These libraries represent globally optimal distributions for a given TIR prediction input data set and the desired library target size. This is exemplified for mCherry and the library sizes 4, 12 and 24 in Fig. 2c. Please note that in this

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**Figure 2 | Rational library reduction by RedLibs.** (a) An externally produced comprehensive input data set for a fully degenerate RBS library (consisting of $a$ nucleotides, here $a = 8$) for a specific gene of interest (goi, here exemplified with mCherry) contains $n = 4^8 = 65,536$ sequence TIR (translation initiation rate) pairs with a strong skew to low TIR levels. (b) Based on this input data set RedLibs compares the TIR distributions of all possible sub-libraries of a user-defined size, which are organized in a database, with a desired target distribution (here: uniform) using the Kolmogorov–Smirnov distance $d_{KS}$. (c) As an output the user receives a list of optimized sub-libraries (i.e., the 10 sub-libraries with the smallest $d_{KS}$) along with the corresponding degenerate sequence for experimental implementation (shown here for mCherry and target sizes of 4, 12 and 24). The respective degenerate and explicit bases are given according to the 15-letter IUPAC nucleotide code. The boxplots over the histograms represent the median (box centre) and first/third quartile (box width) for the respective distribution with 10/90 percentiles displayed as whiskers and outliers as dots.
case RedLibs had to evaluate 4.3, 25.7 and 70.2 million different possible sub-libraries, respectively, a task that cannot be coped with manually. Since RedLibs performs an exhaustive search which is in general a computationally intensive task we designed the underlying algorithm to be suitable for parallelization to minimize computing times and tested its performance for several tasks of different complexities (Supplementary Fig. 1).

The ease of DNA library generation is an important feature of the programme as it facilitates the one-pot generation of a combinatorial RBS library by simple PCR and/or assembly strategies. In summary, the smart composition of the RBS sub-library allows either to reduce the experimental effort while maintaining a high coverage of TIRs (and TIR combinations) or increasing the likelihood of finding meaningful TIR combinations with a given limited number of experiments that can be conducted due to throughput constraints of the experimental assay. The latter might also improve access to complicated pathway optimization approaches in which many pathway steps are balanced and/or high resolutions applied.

**Construction of reduced libraries for fluorescent proteins.** To evaluate the quality of the library distributions produced by our algorithm we conducted a proof of principle experiment in which we concomitantly randomized the RBSs of two fluorescent proteins, superfolder green fluorescent protein (sfGFP) and the red fluorescent protein mCherry (Fig. 2). For this, we constructed plasmid pMJ1 containing the two corresponding genes placed under the control of two copies of the same constitutive promoter in opposite directions separated by a piece of insulating silent DNA to prohibit undesired transcriptional interaction. In front of each gene (7 bp upstream of the start codon) the degenerate RBSs were inserted (Fig. 3a). We applied two different RBS diversification strategies: an unstructured randomization in which six or eight nucleotides were fully randomized ($N_6$ or $N_8$) as well as diversification using smart RBS libraries with target sizes of 4, 12 and 24 members produced by RedLibs to resemble a uniform distribution. We initially performed an in silico screening approach to mimic an actual screen with low throughput by randomly picking 252 TIR pairs for the two fluorescent proteins from the respective libraries (Fig. 2b). As expected for low numbers of picks the fully degenerate libraries deliver only combinations of low TIR levels for both proteins, representing unsatisfactory coverage of the translation level space whose boundaries are defined by the minimum and maximum predicted TIR for each gene. By contrast, the libraries produced by RedLibs achieve good coverage of the entire space already at a small library size (4 × 4) and very good coverages for the 12 × 12 and 24 × 24 libraries indicating a highly improved representation of intermediate and high TIR levels and their combinations. Please note that whereas for the reduced libraries only 48 (4 × 4 library), 432 (12 × 12 library) and 1,726 (24 × 24 library) picks were necessary to achieve a statistical likelihood of $\geq 95\%$ of covering all possible combinations, the fully degenerate libraries would require approximately $5.0 \times 10^7 (N_6 \times N_6)$ library and $1.3 \times 10^{10} (N_8 \times N_8)$ library picks to reach the same coverage\textsuperscript{31}. Based on these in silico results we implemented the same system in vivo and measured the cell-specific green and red fluorescence of 252 clones (three microtiter plates) for each library (Fig. 3c). The experimental results showed a great qualitative resemblance between the in silico predicted and the in vivo observed behaviour for all libraries: whereas candidates picked from the fully degenerate RBS libraries failed to span the whole two-dimensional expression space, the reduced libraries showed a much better coverage for nearly all expression level combinations. Only for combinations of very high expression levels for both proteins no clones were found in the anticipated region (upper right corner of the graphs, Fig. 3c). Deep-sequencing analysis confirmed the presence of sequences that were predicted to lead to combinations of two high TIR values within the libraries which suggested that very high synthesis levels of both proteins are incompatible with the synthesis capacity of the cell. This was confirmed by analysis of a manually cloned mutant containing the highest TIR combination for the sfGFP and mCherry RBSs, which showed a strong downshift in the sfGFP signal as compared with the clone containing the identical RBS for sfGFP but a weak RBS for mCherry (Supplementary Fig. 2) pointing to mutual influences when combining multiple strong RBSs.

**Optimization of violacein production using smart libraries.** To demonstrate the utility of RedLibs for pathway optimization we chose the five-step synthesis pathway for the pigment violacein from L-tryptophan catalysed by VioABEDC. This pathway has been characterized in vitro as well as in vivo in different organisms\textsuperscript{11,32–38}. Due to its branched nature after the intermediate protodeoxyviolaceinic acid and the occurrence of at least two products (violacein and deoxyviolacein) which both require the activity of the same enzyme (VioC) after the branching point (Fig. 4a), we considered it a good test bed for expression level optimization, as the production of violacein with a minimum of deoxyviolacein formation requires on the one hand much VioC to prevent accumulation of proviolacein and to guarantee a certain productivity, but on the other hand little VioC to prevent precursor drainage towards deoxyviolacein. Clearly, a fine-tuned orchestration of VioC and VioD needs to be established to improve the purity of violacein without sacrificing too big a portion of its absolute production level. Furthermore, VioE is a crucial player in determining product spectrum and amount since it directly affects the abundance of protodeoxyviolaceinic acid.

We therefore reasoned that a rationally reduced RBS library would allow tuning the fluxes around the branching point and consequently isolation of clones with a drastically altered product spectrum at a minimal screening effort by randomizing the expression level of the final three enzymes (VioCDE) of the violacein biosynthesis pathway using plasmid pMJ3. Supply of protodeoxyviolaceinic acid as the substrate of the branching point was ensured by fixing the expression of the first two genes (vioAB) from a helper plasmid (pMJ2) with higher copy number (pBR322 ori) when compared to the designated library plasmid for expressing vioCDE (p15A ori) (Fig. 4b). This setup was primarily designed to influence the ratio between the two main products violacein and deoxyviolacein (selectivity) rather than maximizing the overall yield for one or both of the pigments (quantity) with the main goal of producing high purities of violacein, as pure deoxyviolacein could be obtained from a simple vioD knockout strain.

Out of the three initial prediction data sets (one for the RBS of each gene) derived from a full randomization of the SD sequence ($N_4$), RedLibs produced three rationally reduced libraries (target size: 24, maximum number of different combinations in the library: $24^2 = 13,824$) which exhibited a good uniform distribution of predicted TIRs over the whole range of possible TIR levels (Fig. 4b). These libraries were inserted in front of the three genes by extension PCR and the resulting pathway library with concomitantly varied levels for VioC, VioD and VioE was expressed in *Escherichia coli*. A subset of 372 clones ($\sim 2.7\%$) of this library was grown in microtiter plates and the produced pigments (violacein and deoxyviolacein) were semi-quantitatively extracted and quantified by HPLC (Fig. 4c). This first and rough
characterization was applied to obtain an overview of pigment distributions and identify promising combinations for further analysis. Although the exact values for pigment production cannot be faithfully obtained from the semi-quantitative process, the results tentatively suggested that it was possible to tune the ratio of the two pigments quite finely despite the small number of tested clones, as the library exhibited broad variability in several aspects. Of the 372 analysed clones, 325 producers showed a strong diversity in absolute pigment amounts produced. Despite the comparably low throughput of the applied screening assay it was possible to identify clones producing a 240%, 420% and 190% high absolute deoxyviolacein level (dVio1–5), high total pigment level (TP1–5), high selectivity for violacein (%Vio1–5) and high selectivity for deoxyviolacein (%dVio1–5). These 25 clones were re-grown in four independent cultures each and afterwards analysed by quantitative pigment extraction and HPLC. All clones showed superior production behaviour as compared with the parent plasmid (pMJ3 equipped with the initial RBS in front of the three genes as in Addgene plasmid #40782 (ref. 39)). The best clones chosen for improvement in absolute pigment production showed an increase by 34% for violacein, 260% for deoxyviolacein and 44% for total pigment over the parent strain, respectively (Supplementary Fig. 3b). More importantly, the mutants selected for higher selectivity for one pigment showed an increase in violacein fraction from 61 to 81% and in deoxyviolacein fraction from 39 to >99% (i.e., no detectable contamination with violacein) (Fig. 4d). It should be mentioned that, as expected (see above) the clone with the highest purity for deoxyviolacein (%dVio0) was found to contain an in-frame stop codon mutation after 157 residues in the violD gene and can be therefore considered a knockout for the respective enzyme leading to exclusive production of deoxyviolacein.
Analysis of predicted TIRs and improved library design.

After the identification of clones with improved violacein selectivity from the first library we determined the sequence of the corresponding RBSs for \( \text{vioC} \), \( \text{vioD} \) and \( \text{vioE} \) and obtained TIR predictions for each clone by taking the operon context into account\(^2\). In Fig. 5a the predicted TIR values for the five clones with the highest selectivity for violacein (%\( \text{Vio}^1–5 \)) are presented. As mentioned previously this group represents the most challenging objective since a tight balance of pathway enzymes is necessary to obtain high selectivity for violacein. Interestingly, the ratios between the TIRs for VioC and VioD seemed to be exclusively in the lower range within this group and clearly pointed to an excess of VioD over VioC in four of the five cases. By contrast, the TIR for VioE did not seem to be a crucial determinant for high violacein selectivity since it varied significantly among the five analysed clones, both absolute and in relation to the other two TIRs. For the clones with the highest selectivity for deoxyviolacein overall an inverted trend (i.e., TIR\( \text{VioC} > \text{TIR}_{\text{VioD}} \)) was observable (Supplementary Fig. 4).

Figure 4 | Rationally reduced library for optimization of violacein production in \textit{E. coli}. (a) The pigment violacein (VIO) is produced in five heterologous reactions (catalysed by VioABEDC) from \textit{L}-tryptophan. The branched nature of the pathway leads to the formation of other pigments including the main byproduct deoxyviolacein (DVIO). (b) For pathway optimization the genes \( \text{vioC} \), \( \text{vioD} \) and \( \text{vioE} \) were organized in an operon-like structure (plasmid pMJ3). The expression levels were uniformly randomized by implementing a rationally reduced library with a target size of 24 produced by RedLibs out of an initial \( N_0 \) data set for each of the respective proteins. VioA and B were synthesized from a helper plasmid (pMJ2). (c) The rationally reduced RBS library allowed for the creation of a phenotypic variety of clones with distinctly altered product spectra as compared to the library average (solid line) and to the parent clone (pMJ3 with unaltered RBSs, dashed line). With a limited screening effort (372 clones in 96-well microtiter plates) mutants with significantly altered selectivity for the production of VIO and DVIO could be obtained. Please note that note that of the 372 clones analysed 47 were excluded from the figure because they did not produce detectable amounts of either pigment. (d) Quantitative pigment extraction of the five clones with the highest selectivity for either VIO (%\( \text{Vio}^1–5 \)) or DVIO (%\( \text{DVIO}^1–5 \)). Data represents the mean of four independent replicate cultures with standard deviation. *Please note that clone %\( \text{DVIO}^1 \) had an extra stop codon inserted in \( \text{vioD} \) and can therefore be considered a knockout mutant for this gene leading to pure DVIO production (compare a).
Given this observed pattern, there were two options to proceed towards increasing the selectivity further: either to continue screening the original library or the construction of a small new library whose target distribution of TIRs was tailored towards the observed pattern using the RedLibs algorithm. Since exhaustive screening of this first library would have required considerable effort, we decided instead to pursue the latter option and designed a second, improved library to produce clones with low ratios between TIR\text{VioC} and TIR\text{VioD} with a tendency for VioD over VioC. The resulting library should reflect the trends observed in the first library as well as the parent mutant (plasmid pMJ3 with unaltered RBSs, dashed line). (d) From the improved library the clones with the highest violacein purity were obtained (%Vio\text{6–8}) and analysed in detail by quantitative pigment extraction. Bars represent the average violacein fraction of four independent replicate cultures with standard deviation. (e) The RBSs of %Vio\text{6–8} were determined and the corresponding TIRs calculated. Please note that clone %Vio\text{8} was independently found three times in the improved library.

Figure 5 | Improved library design for high violacein selectivity. (a) The TIRs for the clones with the highest violacein selectivity (clones %Vio\text{1–5}; prediction value according to ref. 26) from the initial library suggest a crucial role of the ratio of TIR\text{VioC} and TIR\text{VioD} in the lower stoichiometric range for high violacein selectivity, with a tendency towards a higher value for TIR\text{VioD} than for TIR\text{VioC}. (b) Graphical representation of the rationale behind the second library design by RedLibs. TIRs for VioD are uniformly distributed in the upper range of the accessible TIR space whereas for VioC the lower range is uniformly covered. (c) The resulting library was nearly exhaustively screened revealing a strong tendency to high violacein selectivity relative to the first library as well as the parent mutant (plasmid pMJ3 with unaltered RBSs, dashed line). (d) From the improved library the clones with the highest violacein purity were obtained (%Vio\text{6–8}) and analysed in detail by quantitative pigment extraction. Bars represent the average violacein fraction of four independent replicate cultures with standard deviation. (e) The RBSs of %Vio\text{6–8} were determined and the corresponding TIRs calculated. Please note that clone %Vio\text{8} was independently found three times in the improved library.
most selective clone showing a 1:9 ratio of predicted TIRs (Fig. 5e).

Consequently, RedLibs allowed for the design of a smart two-step optimization scheme which led to efficient improvement of the targeted pathway and can be applied to the iterative synthetic biology design-build-test cycle.

Discussion

Relative and absolute balancing of expression levels within an engineered pathway of interest in a strictly experimental manner remains a major challenge in metabolic engineering. Smartly designed combinatorial libraries, for instance of RBSs, can increase the number of meaningful library variants and are thus a highly useful tool to improve the outcome of the inevitable directed evolution approaches. Here, we develop, test and apply the algorithm RedLibs which allows efficient exploitation of a biophysical model to improve RBS library design. By comparison of cumulative distribution functions RedLibs produces rationally reduced sub-libraries, that (i) are small enough to meet the throughput of the respective screening, (ii) uniformly span the entire range of accessible expression levels (or TIRs) and (iii) are encoded by single degenerate sequences that allow implementation in simple a one-pot cloning procedure. Moreover, in contrast to alternative approaches which use a genetic algorithm to randomly create diversity, RedLibs is capable of identifying the globally optimal libraries within the given data set and will reproducibly deliver identical results for a given task.

Due to the high proportion of meaningful sequences within the libraries produced by RedLibs we were able to demonstrate that it is possible to extract patterns from promising candidate clones in a first step (initial library) and subsequently feed this information back into the algorithm which in turn allowed us to design a second, improved library for a given task to obtain further improved clones at very limited combined screening effort. These iterative heuristics are an important element of the presented work since they allow keeping the overall experimental effort low while still leading to excellent solutions for the ‘sweet spot’ problem.

The identified changes that led to the improved behaviour in the case of violacin selectivity may seem somewhat expected, especially since the tackled pathway is well characterized and the sequential order and topology of the enzymes is known. However, the exact measures that have to be taken to actually guide the flux around the branching point into the desired direction are non-trivial since important parameters like promoter strength, copy number effects, differences in specific activity and Km potential regulation, unknown side-reactions, and so on are unknown. Moreover, RedLibs and the corresponding heuristics that we proposed in this work can likewise be applied to uncharacterized pathway operons. In this case a smart screening strategy might even lead to a better understanding of the respective pathway potential in combination with metabolic flux models.

Finally, we would like to point out that RedLibs is not restricted to uniform target distributions and can easily be adjusted to produce for instance a Gaussian distribution around a user-specified target value. This could for example be useful for fine-tuning purposes in cases where an approximate optimum is known. Moreover, the algorithm is not restricted to RBS prediction sets as input data but can virtually use any sequence-value pair to optimize distributions be it predicted or experimentally determined data.

We anticipate that RedLibs will be a helpful contribution to the aforementioned fields of application in comparison to random approaches as well as to existing methods.

Methods

Computational implementation of RedLibs. RedLibs was developed in the integrated development environment (IDE) XCode (version 4.6) using C++ as programming language. Parallelization of the algorithm was implemented using OpenMP (version 1.4.3). RedLibs uses a database of sequence combinations which were generated using the programming language R (version 2.14.1) in the IDE RStudio (version 0.98.501). For the detailed script please refer to Supplementary Software or https://www.bio.uzh.ch/bpl/software/redlibs. Additionally, the source code was deposited under: https://github.com/dgerngross/RedLibs. The input data for RedLibs was externally generated using the RBS Library Calculator (https://salilab.net/software/) in the ‘Predict: RBS Library’ mode using either six or eight consecutive N bases generating 4,096 or 65,536 sequence TIR pairs. The corresponding RBS sequences including relevant up- and downstream regions for all randomized genes in this work are provided in Supplementary Table 1.

Evaluation of library distributions. RedLibs uses the CDF of each evaluated library and compares it with the cumulative distribution function of the desired target distribution. As a criterion of evaluation the Kolmogorov–Smirnov distance $d_{KS}$ is used which is defined as the maximum absolute difference between the actual cumulative distribution function $F_{	ext{actual}}(x)$ and the target function $F_{\text{target}}(x)$:

$$d_{KS} = \max |F_{\text{actual}}(x) - F_{\text{target}}(x)|$$

Consequently distributions with a high degree of resemblance to the target distribution will exhibit a low $d_{KS}$ value and vice versa. For an exemplary illustrative description of the evaluation process please refer to Supplementary Fig. 5.

Strains and growth media. E. coli TOP10 (F’ mcrA mcrB (mrr-hudRMS-mcrBC) 8080 lacZAM15 lacX74 sup34 recA1 araD139 (ara-leu)7697 galE41 galK16 rpsL(Str8) endA1 l–, Thermo Fisher Scientific) was used for cloning, expression of fluorogenic proteins and for violacin biosynthesis. For the isolation of plasmids with methylation sensitive restriction sites E. coli dam’ dcm’ leuB6 fhuA31 lacY1 tsx78 glnV44 galK2 galT22 mcrA dcm’ hisG4 rfbD1 R(cyb210::Tn10) TetS endA1 rpsL(Str8) Dam3 lac136:Str9 (Cm8) syrA 5 mtl l-- endA1 rpsL(Str8) tetA1 dam1 hsdR2 New England Biolabs) was used. For expression of the fluorogenic proteins sfGFP and mCherry cells were grown in M9 mineral medium supplemented with 10 g l–1 glucose, 0.01% thiamine, 1 mtl l-- 1 trace element solution, 0.1 g l–1 L-valine, 50 mg l–1 i-leucine, 0.03 g l–1 i-isoleucine and 0.15 g l–1 l-valine, 50 mg l–1 kanamycin and 25 mg l–1 streptomycin. For the production of violacin pre-cultures were grown in Luria–Bertani (LB) medium supplemented with 5 g l–1 glucose, 50 mg l–1 kanamycin and 30 mg l–1 carbenicillin. Main cultures were grown in a modified ZYM-5052 medium lacking lactose as autoinduction agent but containing 50 mg l–1 kanamycin and 50 mg l–1 carbenicillin. Induction was performed by the addition of isopropyl–β-D-thiogalactopyranosid (IPTG) to a final concentration of 500 μM.

Vectors for fluorogenic proteins and library construction. Vector pM1 for fluorogenic protein synthesis was constructed according to the Standard European Vector Architecture (SEVA, ref. 46) format and contained a kanamycin resistance cassette, a p15A origin of replication and the default SEVA multiple cloning site. The expression cassette containing the genes for sfGFP and mCherry was obtained by commercial gene synthesis (Life Technologies, Regensburg, Germany, Supplementary Table 2) and cloned into the vector backbone using the restriction enzyme SphI and ligating the fragment into the vector backbone using the restriction enzyme SphI and ligating the fragment into the vector backbone using the restriction enzyme SphI and ligation. For the production of the violacin gene the violacin gene was obtained by commercial gene synthesis (Life Technologies, Regensburg, Germany, Supplementary Table 2) and cloned into the vector backbone using the restriction enzyme SphI and ligating the fragment into the vector backbone using the restriction enzyme SphI and ligation.
In silico screening. The in silico picking experiment to retrieve hypothetical clones from the fluorescent protein libraries was performed using the programming language R (version 2.14.1) in the IDE RStudio (version 0.98.501). Pairwise combinations of predicted TIRs for sfGFP and mCherry were randomly picked from the different libraries at identical probabilities for each TIR value contained in the respective library (e.g., for the library with the size of 4 a 25% probability was applied for each of the four TIRs). For comparability the same number of randomly selected TIR pairs (252 in all experiments) per library were produced as clones analysed in the in vivo experiment. For random picking the ’sample’ (’f’-function, a standard function in R, was used (Supplementary Methods).

Fluorescence measurements. For the quantification of fluorescent proteins 96-deepwell plates containing 1 ml M9 mineral medium per well were inoculated from single colonies and incubated at 37°C and 300 r.p.m. (5 cm shaking diameter) overnight. Afterwards these pre-cultures were used for the inoculation (1/100 dilution) of working plates containing from medium and main cultures were incubated for seven hours (37°C, 300 r.p.m.). Cells were harvested by centrifugation (10 min, 3,220g), resuspended in 1 ml of phosphate buffered saline (PBS), and incubated at 4°C overnight on a table top shaker to ensure full maturation of fluorescent proteins. Subsequently 200 μl of the cell suspensions were transferred into a 96-well flat bottom plate and the optical density at 600 nm (OD600) as well as the fluorescence quantification were performed in a Tecan Infinite M200 plate reader. The quantification of sfGFP and mCherry was carried out at λex = 488 nm/λem = 530 nm and λex = 579 nm/λem = 616 nm, respectively. The fluorescence values were corrected for a well containing PBS only (blank) and normalized to retrieve cell-cell values. To ensure plate to plate comparability reference clones were included in three replicates each for low, fluorescence in both channels (control plasmid lacking the genes for sfGFP and mCherry) as well as for high green and high red fluorescence (strong RBS for sfGFP or mCherry, respectively).

Deep sequencing of fluorescent protein libraries. To confirm the presence of RBSs with high TIR values we performed deep sequencing of RBS libraries on the Illumina MiSeq platform. Sequencing was done at the University of Regensburg (Institute of Chemistry, Metabolism, and Systems Biology) for each of the four TIRs. For comparability the same number of randomly obtained from the different libraries at identical probabilities for each TIR value contained in the respective libraries were pooled and stored at -20°C until quantification of pigments by HPLC.

Violaecin extraction and quantification. Isolation of pigments was performed by ethanol extraction according to a modified version of an earlier protocol48. For sequencing purposes the extracts meant to allow a rough classification of extracts, 500 μl of culture were directly added to 1 ml of pure ethanol and pigments were extracted from the cells for 20 min by vigorous agitation (1,750 strokes min⁻¹) in a homogenizer (2010 Geno/Grinder). After centrifugation (21,130g, 5 min) the supernatant with the pigments was stored at −20°C until quantification. Quantitative extractions were performed in two cycles to ensure full pigment transfer into the extract and accurate quantification: cells from 1 ml of culture were harvested by centrifugation (6,000g, 2 min) and resuspended in 1 ml of pure ethanol. Extraction was performed as before (1,750 strokes min⁻¹, 20 min), the supernatant was collected after centrifugation and the pellet was applied to a second extraction step with 1 ml of fresh ethanol. The two supernatant fractions were pooled and stored at −20°C until quantification of pigments by HPLC.

Chromatographic separation of violacein and deoxyviaceolin was achieved using a ReproSil-Pur C18-AQ column (5 μm, 250 x 4 mm; Dr Maisch GmbH, Germany) on an Agilent 1200 Series HPLC machine with 50% ethanol as a mobile phase applying a flow rate of 1 ml min⁻¹ at 30°C. Violacein and deoxyviaceolin were available as pure standards (BioAustralis Fine Chemicals, Australia) for reference and quantification was carried out by measuring the absorbance in the diode array detector at 575 ± 8 nm (ref. 35).

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Author contributions
M.I. developed the conceptual idea for the project, was responsible for the experimental work, and designed the experiments. D.G. developed the algorithm and contributed to the experiments. S.P. supervised the project. M.I. and S.P. wrote the manuscript.

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