Nature and Strength of Lewis Acid/Base Interaction in Boron and Nitrogen Trihalides

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Abstract: We have quantum chemically investigated the bonding between archetypical Lewis acids and bases. Our state-of-the-art computations on the $X_B N_Y$ Lewis pairs have revealed the origin behind the systematic increase in $B–N$ bond strength as $X$ and $Y$ are varied from $F$ to $Cl$, $Br$, $I$, $H$. For $H_B N_Y$, the bonding trend is driven by the commonly accepted mechanism of donor–acceptor [HOMO (base)–LUMO(acid)] interaction. Interestingly, for $X_B N_H$, the bonding mechanism is determined by the energy required to deform the $B_X$ to the pyramidal geometry it adopts in the adduct. Thus, Lewis acids that can more easily pyramidalize form stronger bonds with Lewis bases. The decrease in the strain energy of pyramidalization on going from $BF_3$ to $BI_3$ is directly caused by the weakening of the $B–X$ bond strength, which stems primarily from the bonding in the plane of the molecule ($\sigma$-like) and not in the $\pi$ system, at variance with the currently accepted mechanism.

Introduction

The chemistry of Lewis acids and bases is rich and can be found in any general chemistry textbook. In his epochal work, Gilbert N. Lewis introduced the concept of electron-pair donor-acceptor complexes, on which the current understanding of Lewis acid/base interactions is based. It defines Lewis acids as chemical species that accepts an electron-pair from a Lewis base to form a Lewis adduct. Thus, the Lewis acidity and basicity scales are associated with the stability of the adducts, that is, relative to a reference, a stronger Lewis acid or Lewis base forms a stronger bounded Lewis complex. The Lewis acid/base chemistry has experienced continuous development since then and has found utility in a wide range of research areas, including catalysis and the recent advent of frustrated Lewis pair chemistry, to name a few.

Due to the ubiquity of Lewis acid/base in chemistry, attempts to rationalize the nature and strength of this interaction abound. The theory of hard and soft acids and bases (HSAB) proposed by Pearson is undoubtedly the most popular qualitative model used to understand this interaction. The HSAB principle uses the intrinsic properties of the interacting species to explain the stability of acid/base complexes, namely, the concept of hardness and softness, which is based on properties such as size, polarizability, and electronegativity. In this model, a hard base (the term “hard” stands for small sized atoms with low polarizability and high electronegativity) would preferentially bind to a hard acid, while a soft base (the term “soft” stands for large sized atoms with high polarizability and low electronegativity) prefers to associate with a soft acid. However, the validity of this model has been questioned, as it has been shown to fail in predicting reactivity of archetypal reactions.

Interestingly, the relative Lewis acidity of boron trihalides with respect to strong bases (e.g., $NH_3$, $NMe_3$) is known to increase along the series $BF_3 < BCl_3 < BBF_3$; however, the opposite trend is observed for the interaction with weak bases (e.g., $N_2$, $CH_2F_2$). This indicates that Lewis acid/base is a rather complex interaction that depends on the entire system, not only on the characteristics of the isolated acids and bases. Over the years, various theories have been proposed to explain the trends in stability of Lewis pairs involving boron trihalides, such as those based on $\pi$-backdonation, the ability to engage in stabilizing orbital interactions or electrostatics, ligand close packing (LCP) model or electrophilicity principle. The decreased Lewis acidity of $BF_3$ towards strong bases, compared to heavier boron trihalides, is widely attributed to a more efficient $\pi$ charge donation from the fluorine lone-pair into the empty $p$ orbital of the boron ($\pi$-backdonation), which reduces the availability of the boron atom to accept an electron pair from the Lewis base. However, it has been shown that the $p(\pi)$-$p(\pi)$ overlap integral and the $p(\pi)$ population at the boron is...
actually smaller for BF₃ than for BCl₃.²¹⁻²⁴ Alternatively, an intuitive argument based on the strength of frontier molecular orbital interactions has been proposed by Bessac and Frenking.²¹² that is, the energy of the LUMO of BX₃ decreases from X = F to Cl and results in more stabilizing orbital interactions with the HOMO of the Lewis base for BCl₃ compared to BF₃. We note that these explanations are universal and neither can explain the reversal in Lewis acidities that is observed for the Lewis complexes between boron trihalides and weak bases.

We aim to illuminate the nature and strength of Lewis acid/base interaction within the conceptual framework provided by Kohn–Sham molecular orbital (KS-MO) theory and ultimately provide a unified framework to understand Lewis pairs. To this end, we investigate the underlying physical mechanism behind the formation of a systematic set of X₃B–NY₃ Lewis pairs (Scheme 1, where X,Y = H, F, Cl, Br, and I). We first explore the archetypical borane–ammonia adduct, H₃B–NH₃, and then separately evaluate the substituent effect on the Lewis acid and Lewis base by varying X,Y from H to F, Cl, Br, and I. To the best of our knowledge, this is the first thorough analysis on the formation of Lewis pairs involving the complete series of nitrogen and boron trihalides. Detailed analysis of the electronic structures and bonding mechanisms enable us to interpret our results in quantitative and chemically meaningful terms, which reveals the role of different components, namely, charge-transfer, electrostatic interaction and also strain energy, in the stability of the Lewis complexes. This demonstrates that, similar to hydrogen bonds,²⁵ Lewis acid/base interaction is a complex interplay of several energy components, whose importance depends on the molecular system and may not be easily captured in simple predictive models.

Methods

Computational Details

All calculations were performed using the Amsterdam Density Functional (ADF) software package.²⁶ Geometries and energies were calculated at the BLYP level of the generalized gradient approximation (GGA); exchange functional developed by Becke (B), and the GGA correlation functional developed by Lee, Yang and Parr (LYP).²⁷ The DFT-D3(BJ) method developed by Grimme and coworkers²⁸ which contains the damping function proposed by Becke and Johnson,²⁹ was used to describe non-local dispersion interactions. Scalar relativistic effects are accounted for using the zeroth-order regular approximation (ZORA).²⁹ Molecular orbitals (MO) were expanded in a large uncontracted set of Slater type orbitals (STOs) containing diffuse functions: TZ2P.³⁰ The basis set is of triple-ζ quality for all atoms and has been augmented with two sets of polarization functions. All electrons were included in the variational process, i.e., no frozen core approximation was applied. An auxiliary set of s, p, d, f, and g STOs was used to fit the molecular density and to represent the Coulomb and exchange potentials accurately in each self-consistent field cycle. The accuracies of the fit scheme (ZLM fit)²² and the integration grid (Becke grid)²⁳ were set to ‘very good’. The Lewis acids were optimized with D₃h symmetry constraints, and the Lewis bases and Lewis adducts were optimized with C₃v symmetry constraints. All optimized structures were confirmed to be true minima though vibrational analyses (no imaginary frequencies). The molecular structures were illustrated using CYLview.³⁰

Activation Strain and Energy Decomposition Analysis

Insight into the nature of Lewis acid/base interaction is obtained by applying the activation strain model (ASM)³ⁱ along the formation of the Lewis adducts. The formation of the Lewis pairs is computationally modelled by decreasing the distance between the boron atom of the Lewis acid and the nitrogen atom of the Lewis base, while other geometry parameters are included in the optimization. Thus, each analysis starts from an optimized Lewis acid and Lewis base at a relatively large distance, then, the B–N distance (rₛₛ) is gradually decreased to a bond length smaller than the equilibrium distance of the Lewis adduct.

The activation strain model of chemical reactivity³³ is a fragment-based approach to understand the energy profile of a chemical process in terms of the original reactants (i.e., the formation of the dimer from monomers). Thus, the overall bond energy ΔE(Ξ) is decomposed into the respective total strain and interaction energy, ΔEstrain(Ξ) and ΔEint(Ξ), and project these values onto the reaction coordinate ξ (in this case, rₛₛ) [Eq. (1)].

$$\Delta E(\xi) = \Delta E_{\text{strain}}(\xi) + \Delta E_{\text{int}}(\xi)$$  

(1)

In this equation, the total strain energy ΔEstrain(Ξ) is the penalty that needs to be paid to deform the reactants from their equilibrium structure to the geometry they adopt in the complex at point ξ of the reaction coordinate. On the other hand, the interaction energy ΔEint(Ξ) accounts for all the chemical interactions that occur between the deformed fragments along the reaction coordinate. The total strain energy can, in turn, be further decomposed into the strain energies corresponding to the deformation of the Lewis acid ΔEstrain(BX₃)(Ξ) as well as from the Lewis base ΔEstrain(NY₃)(Ξ) [Eq. (2)].

$$\Delta E_{\text{strain}}(\xi) = \Delta E_{\text{strain}}(\text{BX}_3)(\xi) + \Delta E_{\text{strain}}(\text{NY}_3)(\xi)$$  

(2)

The interaction energy between the deformed fragments is further analyzed in terms of quantitative Kohn–Sham molecular orbital (KS-MO) theory in combination with a canonical energy decomposition analysis (EDA).³⁵ The EDA decomposes the ΔEint(Ξ) into the following four physically meaningful energy terms [Eq. (3)].

$$\Delta E_{\text{int}}(\xi) = \Delta V_{\text{elstat}}(\xi) + \Delta E_{\text{Pauli}}(\xi) + \Delta E_{\text{Pauli}}(\xi) + \Delta E_{\text{disp}}(\xi)$$  

(3)

Herein, ΔV_{elstat}(Ξ) is the classical electrostatic interaction between the unperturbed charge distributions of the (deformed) fragments and is usually attractive. The Pauli repulsion ΔE_{Pauli}(Ξ) comprises the destabilizing interaction between occupied closed-shell orbitals of both fragments due to the Pauli principle. The orbital interaction energy ΔE_{Pauli}(Ξ) accounts for polarization and charge transfer between the fragments, such as HOMO–LUMO interactions. It can be decomposed into the contributions from each irreducible

![Scheme 1. Formation of the Lewis pairs analyzed in this work.](image-url)
Voronoi Deformation Density (VDD) charges

The atomic charge distribution was analyzed by using the Voronoi Deformation Density (VDD) method.\(^\text{29}\) The VDD method partitions the space into so-called Voronoi cells, which are non-overlapping regions of space that are closer to nucleus A than to any other nucleus. The charge distribution is determined by taking a fictitious promolecule as reference point, in which the electron density is simply the superposition of the atomic electronic densities. The charge in density in the Voronoi cell when going from this promolecule to the final molecular density of the interacting system is associated with the VDD atomic charge \(Q\). Thus, the VDD atomic charge \(Q_{\text{VDD}}\) of atom A is given by:

\[
Q_{\text{VDD}} = -\int_{\text{Voronoi cell of } A} \left( \rho(r) - \rho_{\text{promolecule}}(r) \right) dr
\]

(5)

Instead of computing the amount of charge contained in an atomic volume, we compute the flow of charge from one atom to the other upon formation of the molecule. The physical interpretation is therefore straightforward. A positive atomic charge \(Q\) corresponds to the loss of electrons, whereas a negative atomic charge \(Q\) is associated with the gain of electrons in the Voronoi cell of atom A.

Results and Discussion

Structures and bond strengths

In this section, the geometries and bond energies of the \(\text{X}_3\text{B}–\text{NY}_3\) Lewis pairs (\(\text{XY} = \text{H}, \text{F}, \text{Cl}, \text{Br}, \text{I}\)) are discussed. The results are summarized in Figure 1 (full structural data is provided in Table S1 in the Supporting Information). As \(\text{BX}_3\) and \(\text{NY}_3\) approach each other to form the Lewis adduct, the Lewis acid must pyramidalize from its trigonal planar equilibrium geometry, that is, the \(\theta_{\text{B-H-X}}\) angle decreases and the \(r_{\text{B-H}}\) bond length increases (Table S1). This effect is much less pronounced in the Lewis base, as it already has a pyramidal equilibrium geometry and undergoes almost no deformation upon complexation. Our computed bond lengths and angles of borane–ammonia (i.e., \(\text{H}_3\text{B}–\text{NH}_3\)) are in very good agreement with existing experimental data\(^{10}\) (in parenthesis): \(r_{\text{B-H}}\) bond length of 1.675 Å (1.657 Å), \(r_{\text{B-N}}\) bond length of 1.211 Å (1.216 Å), \(r_{\text{N-H}}\) bond length of 1.022 Å (1.014 Å), \(\theta_{\text{N-H-B}}\) angle of 113.8° (113.8°), and \(\theta_{\text{N-H-N}}\) angle of 107.8° (108.7°).

The expected trends in Lewis adduct stabilities are nicely reproduced by our DFT computations at ZORA-BLYP-D3(BJ)/TZ2P. Borane–ammonia forms the strongest bond complex in our series of Lewis pairs (\(\Delta E = -29.5 \text{ kcal mol}^{-1}\)). Upon substitution of the hydrogen atoms on the Lewis acid or Lewis base with halogen atoms, the energy of formation of the Lewis adduct \(\Delta E\) decreases in strength, i.e., becomes less stabilizing, along the series: \(\text{H}, \text{I}, \text{Br}, \text{Cl}, \text{F}\). The bond enthalpies at 298 K (\(\Delta H_{298.15}\)) show the same trends as the electronic bond energies \(\Delta E\) (see supporting methods and Table S1 in the Supporting Information). In the following sections, we partition the Lewis pairs into three sets: 1) \(\text{H}_3\text{B}–\text{NH}_3\), 2) \(\text{X}_3\text{B}–\text{NH}_3\), and 3) \(\text{H}_3\text{B}–\text{NY}_3\) (where \(\text{XY} = \text{F}, \text{Cl, Br, and I}\)), and provide a unified model to rationalize the strength of the Lewis pair bond through detailed analyses of the electronic structure and bonding mechanism.

Borane-Ammonia

The activation strain model and energy decomposition analysis diagrams of the borane–ammonia adduct are shown in Figure 2. From Figure 2a, it can be easily seen that the energy profile in \(\Delta E\) curve along the newly forming \(\text{B}–\text{N}\) bond is determined by the interaction energy \(\Delta E_{\text{int}}\) which becomes destabilizing only at very short \(\text{B}–\text{N}\) bond distance (smaller than \(r_{\text{B-N}} < 1.230 \text{ Å}\)). The strain energy \(\Delta E_{\text{strain}}\) on the other hand, becomes increasingly destabilizing as the internuclear distance decreases. The destabilizing \(\Delta E_{\text{strain}}\) stems mostly from the deformation of the Lewis acid, \(\text{BH}_3\), from its planar equilibrium geometry to the pyramidal geometry it adopts in the complex. Note that the \(\text{BH}_3\) strain energy curve \(\Delta E_{\text{strain-BH}_3}\) coincides with the total strain energy curve \(\Delta E_{\text{strain}}\), whereas the \(\text{NH}_3\) strain energy curve \(\Delta E_{\text{strain-NH}_3}\) is flat all along the reaction coordinate.

Since the interaction energy plays a critical role on the formation of the \(\text{H}_3\text{B}–\text{NH}_3\) Lewis pair, we further decomposed \(\Delta E_{\text{int}}\) into four physically meaningful terms according to Eq. (3). The results of this energy decomposition analysis (EDA) are shown in Figure 2b. This graph shows us a quite straightforward picture. The \(\Delta E_{\text{int}}\) is equally stabilized by orbital and electrostatic interactions, the \(\Delta E_{\text{oi}}\) and \(\Delta V_{\text{elstat}}\) curves nearly coincide at all \(\text{B}–\text{N}\) bond distances shown. Both terms become more stabilizing as the fragment separation decreases and the bond begins to form, because of the increase in both HOMO–LUMO orbital overlap and charge penetration of nuclei with electron clouds. The stabilizing effect of \(\Delta E_{\text{oi}}\) and \(\Delta V_{\text{elstat}}\) is, however, opposed by the Pauli repulsion \(\Delta E_{\text{pauli}}\) term. Note that at a \(\text{B}–\text{N}\) separation shorter than the equilibrium bond length, the upward slope of the \(\Delta E_{\text{pauli}}\) curve is larger than the downward slope of the \(\Delta E_{\text{oi}}\) and \(\Delta V_{\text{elstat}}\) curves, which is the reason behind the destabilization of \(\Delta E_{\text{int}}\) at short internuclear distance.\(^{11}\) The dispersion energy \(\Delta E_{\text{disp}}\) on the other hand, remains nearly constant at any point along \(r_{\text{B-N}}\).

Thus, electrostatic and orbital interactions are the main contributors to the formation of the \(\text{H}_3\text{B}–\text{NH}_3\) Lewis pair. To understand the origin of the stabilizing \(\Delta E_{\text{oi}}\) and \(\Delta V_{\text{elstat}}\), we have analyzed the molecular orbital (MO) diagram of the fragment molecular orbitals (FMOs) and the electrostatic potential surface of each fragment, respectively.\(^{12}\) To ensure that our results are not skewed by the fact that the Lewis
adducts have different equilibrium bond lengths, analysis of all Lewis pairs will be performed at the same $r_{B-N}$ distance of 1.687 Å, near to the equilibrium bond distance of borane–ammonia. Energies at consistent geometry for the $\text{H}_2\text{B}–\text{NH}_3$ adduct are shown in Figure 2c.

Figure 3a shows that $\Delta E_{oi}$ can be rationalized in terms of the well-known [HOMO(base)–LUMO(acid)] interaction between the

Figure 1. Equilibrium geometries (in Å, deg.) of the a) $\text{BX}_3$ Lewis acids, b) $\text{X}_3\text{B–NY}_3$ Lewis adducts, and c) $\text{NY}_3$ Lewis bases ($\text{X,Y} = \text{H, F, Cl, Br, and I}$), along with the electronic bond energies $\Delta E$ (in kcal mol$^{-1}$) computed at ZORA-BLYP-D3(BJ)/TZ2P.
filled N 2p orbital of the Lewis base with the empty B 2p orbital of the Lewis acid (see Figure 3b). This interaction has favorable orbital energy gap ($\Delta \varepsilon = 2.5$ eV) and overlap ($\langle \text{HOMO} | \text{LUMO} \rangle = 0.36$). Furthermore, inspection of the electrostatic potential surfaces illustrated in Figure 3c and atomic charges in Figure 3d reveals that accumulation of positive charge around the boron atom of the electron-deficient Lewis acid and negative charge around the nitrogen atom of the electron-rich Lewis base are responsible for the stabilizing $\Delta V_{\text{elstat}}$.

In summary, the EDA along the forming $\text{H}_3\text{B}-\text{NH}_3$ Lewis pair demonstrates that the attractive interaction between the BH$_3$ Lewis acid and the NH$_3$ Lewis base has a stabilizing covalent character that is the same magnitude as the electrostatic character, both can be easily understood in terms of simple chemical arguments. Our results, so far, conform to and agree with the current picture presented in the literature.$^{[6d,e,i]}$ In the coming next sections, we extend our analysis to study the stability of Lewis adducts of halogenated Lewis acids and Lewis bases.

### Halogenated Lewis Acids

Next, we turn to the analysis of the formation of the Lewis pairs between boron trihalides and ammonia. The activation strain model and energy decomposition analysis diagrams for the $\text{X}_3\text{B}-\text{NH}_3$ Lewis pairs (where X = F, Cl, Br, and I) are shown in Figure 4. In line with the expected Lewis acidities,$^{[9c]}$ BI$_3$ forms the strongest complex with ammonia and the energy of formation of the Lewis adduct $\Delta E$ decreases in strength, i.e., becomes less stabilizing, along the series: BI$_3$, BBr$_3$, BCl$_3$, BF$_3$. However, in contrast with the commonly accepted view of Lewis acid/base interaction, the stronger bond energy does not originate from the more stabilizing interaction energy, but from...
the less destabilizing strain energy \(^{(12a,33)}\). In general, \(\Delta E_{\text{strain}}\) is less destabilizing for the Lewis complex involving Bi and becomes increasingly destabilizing along the series \(\text{Bi} < \text{BBr} < \text{BCl} < \text{BF}\). On the other hand, \(\Delta E_{\text{int}}\) is nearly the same for all Lewis adducts and does not follow a systematic trend. If covalent interactions would be the decisive factor for the observed Lewis pair stabilities, one would expect that the trend in \(\Delta E_{\text{int}}\) along the boron trihalides also hold for the trend in \(\Delta E\); but this is not the case. We discuss these findings in more details below.

The same conclusion can be drawn at consistent geometries (\(r_{B-N} = 1.687\ \text{Å}\), see Table 1; the EDA data is given in Table S2). The values of \(\Delta E_{\text{int}}\) are of the same order of magnitude as in borane–ammonia, ca. 41 kcal mol\(^{-1}\); while the \(\Delta E_{\text{strain}}\) is significantly larger for the boron trihalides and accounts for 12.2 and 22.3 kcal mol\(^{-1}\) for H\(_3\)B–NH\(_3\) and F\(_3\)B–NH\(_3\), respectively. The \(\Delta E_{\text{strain}}\) results predominantly from the deformation of the Lewis acid \(\Delta E_{\text{strain,BX}}\). Nevertheless, there is no clear correlation of \(\Delta E_{\text{strain,BX}}\) with any geometrical change. The pyramidalization angle \(\Delta \theta_{\text{pyr,BX}}\) is very similar for all Lewis acids and the B–X bond stretching \(\Delta r_{B-X}\) has a reversed trend that from \(\Delta E_{\text{strain,BX}}, \text{i.e., the } \Delta r_{B-X} \text{ increases as } X \text{ goes from } F \text{ to } I \) (see Table 1).

In order to pinpoint the origin of the observed strain energy of the boron trihalides, we have carried out a subsequent analysis on the BX\(_3\) fragment. This time we decompose the \(\Delta E_{\text{strain,BX}}\) term into the individual strain energies associated with the bending of the \(\theta_{x-y-z}\) angle (\(\Delta E_{\text{strain,x}}\)) and the B–X bond stretch (\(\Delta E_{\text{strain}}\)), as schematically illustrated in Table 2. First, the BX\(_3\) is pyramidalized with a fixed \(r_{B-X}\), taken from the respective planar equilibrium geometry, and, next, the \(r_{B-X}\) bond is allowed to relax to the one it has in the consistent geometry

![Figure 4](image-url)

**Figure 4.** a) Activation strain model and b) energy decomposition analysis of the X\(_3\)B–NH\(_3\) Lewis pairs projected onto the forming B–N bond distance (where \(X = F, Cl, Br, \text{ and I}\)) computed at ZORA-BLYP-D3(BJ)/TZ2P. Dispersion energy \(\Delta E_{\text{disp}}\) not shown, see Table S2 for data at consistent geometries.

| Lewis acid | \(\Delta r_{x-y}\) | \(\Delta \theta_{x-y-z}\) | \(\Delta \theta_{\text{pyr,BX}}\) | \(\Delta E_{\text{strain,BX}}\) | \(\Delta E_{\text{strain}}\) | \(\Delta E_{\text{int}}\) | \(\Delta E_{\text{disp}}\) |
|------------|------------------|------------------|------------------|------------------|------------------|------------------|------------------|
| BF\(_3\)   | 0.060            | 0.001            | −17.2            | 5.7              | −18.3            | −40.6            | 22.3             |
| BCl\(_3\)  | 0.089            | 0.002            | −18.0            | 7.4              | −21.0            | −41.3            | 20.3             |
| BBr\(_3\)  | 0.096            | 0.003            | −18.0            | 7.7              | −24.5            | −42.6            | 18.1             |
| Bi\(_3\)   | 0.103            | 0.004            | −17.6            | 7.5              | −25.6            | −41.2            | 15.5             |

[a] Computed at ZORA-BLYP-D3(BJ)/TZ2P, geometrical data relative to the separate reactants. [b] Pyramidalization angle defined as the sum of the three \(\theta_{x-y-z}\) and \(\theta_{x-y-z,y-z}\) angles for BX\(_3\) and NH\(_3\), respectively.
of the Lewis pair. The energy associated with each geometrical deformation is presented in Table 2. The majority of the strain energy originates from the bending of the $\theta_{B-X}$ angle and the trends in $\Delta E_{\text{strain,0}}$ follow exactly the trends of the total strain of the Lewis acid $\Delta E_{\text{strain,0}}$, that is, it is larger for BF$_3$ and smaller for BBr$_3$. The same trend can be observed if we analyze the other boron trihalides. Why then does BX$_3$ become easier to bend to the same extent along the series $X = F, Cl, Br, and I$?

To answer to this question, we must understand exactly how the electronic structure of the Lewis acid changes upon pyramidalization (that is, bending and elongation). The rise in energy associated with the deformation of BX$_3$ (i.e., $\Delta E_{\text{strain,BX$_3$}}$) could stem from two distinct factors: i) the bonding between central boron and halogen ligands becomes less stabilizing in the pyramidal geometry; and ii) there is an increase in the repulsion among the halogens as BX$_3$ deforms. Therefore, we have further decomposed the $\Delta E_{\text{strain,BX$_3$}}$ in terms of the interaction energy between B and X$_i$ ($\Delta E_{\text{int,b-X$_i$}}$) and among the three X ($\Delta E_{\text{int,x-x-x}}$), more specifically, in terms of the change in both energy terms as BX$_3$ deforms from the planar to the pyramidal geometry (Table 3; see supporting methods for a complete derivation).

Put simply, the interaction energy $\Delta E_{\text{int,x-x-x}}$ corresponds to the formation of the $\langle X^i \rangle$ fragment in its quartet valence configuration and in the geometry which it acquires in the overall molecule, and the interaction energy $\Delta E_{\text{int,b-X$_i$}}$ corresponds to the actual energy change when the prepared B–sp$^2$ and $\langle X^i \rangle$ fragments are combined to form the BX$_3$ (planar or pyramidal). As BX$_3$ goes from one geometry to the other, the change in interaction energy is written as $\Delta \Delta E_{\text{int}}$. Thus, the $\Delta \Delta E_{\text{int,b-X$_i$}}$ and $\Delta \Delta E_{\text{int,x-x-x}}$ are, respectively, the change in both interaction energy terms when BX$_3$ goes from the planar to the pyramidal geometry and sum to $\Delta \Delta E_{\text{strain,BX$_3$}}$ (see Table 3). Here, positive values of $\Delta \Delta E_{\text{int}}$ indicate that the interaction energy opposes pyramidalization, while negative values indicate that it favors pyramidalization of the Lewis acid.

The most striking result in Table 3 is that the interaction energy between the halogens, which is predominantly repulsive (see Table S4), becomes less destabilizing in the pyramidal geometry (i.e., $\Delta \Delta E_{\text{int,x-x-x}}$ is negative) and, thus, favors the pyramidalization of the Lewis acid. This is because when the $r_{B-X}$ bond elongates, the halogens are actually farther removed from each other in the pyramidal than in the planar geometry (see $\Delta \Delta E_{\text{int,b-X$_i$}}$ in Table S3). This means that $\Delta \Delta E_{\text{int,b-X$_i$}}$ determines the trends in $\Delta \Delta E_{\text{strain,BX$_3$}}$, as clearly observed from Table 3. Along X = F to I, $\Delta \Delta E_{\text{strain,BX$_3$}}$ varies from 22.2 to 15.3 kcal mol$^{-1}$ and $\Delta \Delta E_{\text{int,b-X$_i$}}$ varies from 27.0 to 20.4 kcal mol$^{-1}$.

### Table 3. Change in the energy decomposition analysis terms (in kcal mol$^{-1}$) associated with the deformation of the BX$_3$ Lewis acids from the planar to the pyramidal geometry$^{[a]}$ (where X = F, Cl, Br, and I).$^{[b]}$

| Lewis acid | $\Delta E_{\text{strain,BX$_3$}}$ | $\Delta \Delta E_{\text{int,b-X$_i$}}$ | $\Delta \Delta E_{\text{int,x-x-x}}$ | $\Delta \Delta E_{\text{int,b-X$_i$}}$ | $\Delta \Delta E_{\text{int,x-x-x}}$ | $\Delta \Delta E_{\text{int,b-X$_i$}}$ | $\Delta \Delta E_{\text{int,x-x-x}}$ |
|-----------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| BF$_3$    | 22.2            | -4.8            | 27.0            | 74.7            | -142.5          | 94.7            | 27.1            |
| BCI$_3$   | 20.1            | -6.5            | 26.6            | 95.8            | -126.0          | 56.8            | 13.5            |
| BBr$_3$   | 17.8            | -5.7            | 23.5            | 102.5           | -122.0          | 43.1            | 8.5             |
| Bi$_3$    | 15.3            | -5.1            | 20.4            | 99.3            | -112.1          | 33.2            | 5.8             |

[a] Geometry adopted in the complex with a B–N distance of 1.687 Å of the X$_B$–NH$_3$ Lewis pairs. [b] Computed at ZORA-BLYP-D3(BJ)/TZ2P.

![Diagram](image-url)
energy between the boron and the halogens is less stabilizing in the pyramidal than in the planar geometry \(\text{i.e., } \Delta \varepsilon_{\text{BD}}(\text{E}X)\text{ is positive} \) and, thus, opposes the pyramidalization of the Lewis acid. This loss in stabilization correlates to the difficulty to pyramidalize the Lewis acid, that is, a larger \(\Delta \varepsilon_{\text{BD}}(\text{E}X)\text{ translates to a larger } \Delta \varepsilon_{\text{strain,BX}}\).

To obtain insight into the different contributors to the interaction energy we have again employed the EDA scheme\(^{[27]}\) (see Table 3, full data is provided in Table S5). It can be seen that the trend in \(\Delta \varepsilon_{\text{int,BX}}\) is dictated by the orbital interactions \(\Delta \varepsilon_{\text{oi,BX}}\). Both \(\Delta \varepsilon_{\text{oi,BX}}\) and \(\Delta \varepsilon_{\text{oi,BX}}\) oppose pyramidalization of the Lewis acid \(\text{i.e., } \Delta \varepsilon_{\text{BD}}\text{ are positive} \) and decrease in magnitude from \(\text{BF}_3\) to \(\text{Bi}_3\). Along \(X = F\) to \(I\), \(\Delta \varepsilon_{\text{B-X,Y}}\) varies from a value of 94.7 to 33.2 kcal mol\(^{-1}\). Note that the electrostatic interaction also opposes pyramidalization \(\text{i.e., } \Delta \varepsilon_{\text{elstat,BX}}\) but it increases from \(\text{BF}_3\) to \(\text{Bi}_3\), therefore, not following the trend in \(\Delta \varepsilon_{\text{int,BX}}\). Interestingly, the Pauli repulsion term favors pyramidalization \(\text{i.e., } \Delta \varepsilon_{\text{Pauli,BX}}\) because it goes with an elongation of the \(\text{r}_{\text{e-X}}\) bond in the pyramidal geometry, which becomes longer from \(\text{BF}_3\) to \(\text{Bi}_3\). Therefore, in a sense, \(\Delta \varepsilon_{\text{strain,BX}}\) and \(\Delta \varepsilon_{\text{Pauli,BX}}\) work together against the observed trend in \(\Delta \varepsilon_{\text{int,BX}}\). Finally, the dispersion term, \(\Delta \varepsilon_{\text{disp,BX}}\) is the same at both geometries \(\text{i.e., } \Delta \varepsilon_{\text{disp,BX}} = 0\) and is not provided in Table 3).

Figure 5 shows the MO diagram of the main orbital interactions between \(\text{X}^1\) and \(\text{B}-\text{sp}^2\) in the \(e_1\) and \(a_1\) representations (the complete MO diagram with all valence orbitals is provided in Figure S3). We now address why the covalent component of the interaction between \(B\) and \(X\) is less stabilizing in the pyramidal geometry, that is, \(\Delta \varepsilon_{\text{oi,BX}}\) is positive, and how it determines the trend in \(\Delta \varepsilon_{\text{strain,BX}}\). Most of this effect originates from the orbital interactions in the \(e_1\) irreducible representation (see Table 3), which corresponds to the bonding in the plane of the molecule \(\pi\)-like bonding). Interestingly, the total stabilizing orbital interactions \(\Delta \varepsilon_{\text{oi,BX}}\) is provided by nearly \(70\% \Delta \varepsilon_{\text{oi,BX}}\) and \(30\% \Delta \varepsilon_{\text{oi,BX}}\) (the contribution from \(\Delta \varepsilon_{\text{oi,BX}}\) is very small, see Table S4). This is in contrast to the common belief that the strength of the \(\text{B-X}\) bond arises from the overlap in the \(\pi\)-system \(\text{i.e., } \Delta \varepsilon_{\text{oi,BX}}\) representation), between the filled \(\pi\)-orbitals of the halogen and the empty \(p\)-orbital of boron.\(^{[29]}\)

In planar \(\text{BX}_3\) (Figure 5a left), two electron pair bonds are formed in the \(e_1\) irreducible representation \(\text{ne}_1\pm 2\text{p}_\alpha\) and \(\text{ne}_1\pm 2\text{p}_\beta\), where \(\text{ne}_1\) is a combination of the \(n\)-orbitals in the \(xy\) plane of the halogen atoms. The degenerated singly occupied \(\text{ne}_1\) orbitals show the well-known energy on descending group 17 in the periodic table,\(^{[30]}\) from \(-12.7\) to \(-8.0\) eV as \(X\) goes from \(F\) to \(I\), associated with the decreasing electronegativity of \(X\).\(^{[30]}\) As the fragments combine to form \(\text{BX}_3\), the electrons are stabilized in the bonding molecular orbitals and this stabilization correlates well with the energy of the \(\text{X}^1\) fragment orbitals, in line with the order of strength of the \(\text{B-X}\) bond.\(^{[31]}\) Upon pyramidalization, there is a decrease in the orbital overlap between \(\text{ne}_1\) and \(2\text{p}_X\) for all \(\text{BX}_3\) (see Table S4), resulting in the less stabilizing \(\Delta \varepsilon_{\text{oi,BX}}\). Furthermore, pyramidalization also results in destabilization of the \(\text{ne}_1\) orbitals of the \(\text{X}^3\) fragment and, most important, in the bonding molecular orbitals of \(\text{BX}_3\) (Figure 5a right). Interestingly, the destabilization of the bonding molecular orbitals shows the same trend as the \(\Delta \varepsilon_{\text{strain,BX}}\) that is, it decreases along the series \(X = F, Cl, Br, I\) \((\Delta \varepsilon = 0.4, 0.3, 0.3, \text{and } 0.2 \text{ eV} \text{ for } \text{BF}_3, \text{BCl}_3, \text{BBBr}_3, \text{and } \text{Bi}_3\) respectively). Similar effect occurs for orbital interactions in the \(a_1\) representation (see Figure 5b). Thus, as the boron trihalides deform to the same extent, the destabilization in the molecular orbitals of \(\text{BF}_3\) is larger. The \(\text{F}^2\) is more strongly bound to the central boron atom, therefore, the decrease in the strain energy from \(\text{BF}_3\) to \(\text{Bi}_3\) can be ascribed to the amount of energy required to distort a weaker bond. In other words, it requires less energy to deform \(\text{Bi}_3\) than \(\text{BF}_3\) because the \(B-\text{I}\) bond is weaker than the \(B-F\) bond.

At last, we comment on the role of the orbital interactions between the Lewis acid and the Lewis base to the stability of the \(\text{X},\text{B}-\text{NH}_3\) Lewis pairs (where \(X = F, Cl, Br, \text{and } I\), which is the widely accepted rationale to explain the Lewis acidity of boron trihalides.\(^{[31]}\) Our EDA results (Figure 4b and Table S2), indeed, demonstrate that \(\Delta \varepsilon_{\text{el}}\) follows the trend in \(\Delta \varepsilon\) that is, it becomes more stabilizing from \(\text{F},\text{B}-\text{H}_3\) to \(\text{I},\text{B}-\text{NH}_3\). The trends in \(\Delta \varepsilon\) can be ascribed to the energy of the LUMO of \(\text{BX}_3\) that decreases in energy from \(\text{BF}_3\) to \(\text{Bi}_3\) (see Figure 5b), resulting in more stabilizing orbital interactions, in line with the results by Bessac and Frenking.\(^{[31]}\) However, the stabilizing effect of \(\Delta \varepsilon_{\text{el}}\) (and also \(\Delta \varepsilon_{\text{int}}\)) is counteracted by a strong Pauli repulsion \(\Delta \varepsilon_{\text{Pauli,BX}}\) that leads to a similar \(\Delta \varepsilon_{\text{int}}\) for all Lewis adducts (see Figure 4b). We again emphasize that it is crucial to compare the Lewis adducts at a consistent geometry, that is, the same \(r_{\text{NO}},\text{H}\) bond length, because the energy components are highly dependent on the bond distance.\(^{[32]}\) Data at the equilibrium geometries (Table S1) shows that the strain energy of \(\text{BF}_3\) is smaller than \(\text{BCl}_3\), but this is just because of the longer \(r_{\text{NO},\text{H}}\) bond distance in the Lewis pair with the former. Analysis at the consistent geometries (Table 1) shows that the trends in bond energy \(\Delta \varepsilon\) can solely be assigned to the strain energy of the Lewis acid \(\Delta \varepsilon_{\text{strain,BX}}\); not to the interaction energy \(\Delta \varepsilon_{\text{int}}\).

We conclude that the more destabilizing strain energy along the series \(\text{Bi}_3 < \text{BBBr}_3 < \text{BCl}_3 < \text{BF}_3\) leads to less stable \(\text{X},\text{B}-\text{NH}_3\) Lewis pairs (where \(X = F, Cl, Br, \text{and } I\), due to a loss in stabilization of the bonding interactions between the central boron and the halogen ligands as the \(\text{BX}_3\) goes from the planar to the pyramidal geometry. This effect is most pronounced for \(\text{BF}_3\) because the \(B-\text{F}\) bond is the strongest in our series of boron trihalides. These general observations also explain why a reversed trend is observed for the interaction of boron trihalides with weak bases\(^{[33]}\) weak bases induce small distortion of \(\text{BX}_3\) from its planar equilibrium geometry that allows the interaction energy to dominate and govern the bonding of these Lewis pairs.

**Halogenated Lewis Bases**

Finally, we turn our attention to the formation of Lewis adducts between borane and nitrogen trihalides. The activation strain model and energy decomposition analysis diagrams for the
Lewis pairs (where $Y = F, Cl, Br, and I$) are shown in Figure 6, whereas data at consistent geometries is summarized in Table 4. The NI$_3$ forms the strongest complex with borane and the energy of formation of the Lewis adduct $\Delta E$ decreases in strength, i.e., becomes less stabilizing, along the series: NI$_3$, NBr$_3$, NCl$_3$, NF$_3$. Trends in $\Delta E$ curves originate solely from a more stabilizing interaction energy $\Delta E_{\text{int}}$. Note that the strain energy $\Delta E_{\text{strain}}$ curves show a reversed trend, overruled by the trend in $\Delta E_{\text{int}}$, namely, NF$_3$ has a less destabilizing $\Delta E_{\text{strain}}$ than NI$_3$. Therefore, similar to borane–ammonia, the relative stability of the H$_3$B–NY$_3$ Lewis pairs is determined by $\Delta E_{\text{int}}$.

**Figure 5.** Orbital interaction scheme for planar and pyramidal BX$_3$ (where $X = F, Cl, Br, and I$) in the a) $e_1$ and b) $a_1$ irreducible representations of the $C_3v$ symmetry computed at ZORA-BLYP-D3(BJ)/TZ2P.

**Table 4.** Activation strain model and energy decomposition analysis terms (in kcal mol$^{-1}$) computed at consistent geometries with a forming B–N distance of 1.687 Å of the H$_3$B–NY$_3$ Lewis pairs (where $Y = F, Cl, Br, and I$).

| Lewis base | $\Delta E$ | $\Delta E_{\text{strain}}$ | $\Delta E_{\text{int}}$ | $\Delta V_{\text{elstat}}$ | $\Delta E_{\text{Pauli}}$ | $\Delta E_{\text{oi}}$ | $\Delta E_{\text{disp}}$ |
|-----------|-----------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| NF$_3$    | -10.5     | 6.5               | -16.9             | -39.6             | 88.2              | -63.0             | -2.5              |
| NCl$_3$   | -14.0     | 7.8               | -21.8             | -46.0             | 94.6              | -65.2             | -5.2              |
| NBr$_3$   | -16.3     | 8.4               | -24.7             | -43.6             | 94.2              | -69.2             | -6.1              |
| NI$_3$    | -18.8     | 9.6               | -28.3             | -48.9             | 99.4              | -71.5             | -7.3              |

[a] Computed at ZORA-BLYP-D3(BJ)/TZ2P.
The observed trend in $\Delta E_{\text{int}}$ curves is given by the orbital interaction $\Delta E_{\text{int}}$ curves, that is most stabilizing for the Lewis complex with $N_j$ and decreases in strength along the series $N_3$, $NBr_3$, $NCl_3$, $NF_3$, $NI_3$ from $N_3$ to $NF_3$, at the consistent geometry (see Table 4), $\Delta E_{\text{int}}$ varies from a value of $-28.3$ to $-16.9$ kcal mol$^{-1}$ and $\Delta E_{\text{disp}}$ varies from a value of $-71.5$ to $-63.0$ kcal mol$^{-1}$. This is paralleled by a decrease of Pauli repulsion, that varies from a value of $99.4$ to $88.2$ kcal mol$^{-1}$ from $N_j$ to $NF_j$, as reflected by the decreasing number of core electrons and diffuse orbitals as the halogen decreases in size. Trends in $\Delta V_{\text{elstat}}$ on the other hand, are not exactly systematic along the Lewis bases. They are partially inverted and decreases in strength along the series $N_3$, $NCl_3$, $NBr_3$, $NF_3$, $NI_3$. Finally, the dispersion energy $\Delta E_{\text{disp}}$ has the smallest contribution to $\Delta E_{\text{int}}$ (not shown in Figure 6, see Table 4 for data at consistent geometries).

Formation of the $H_jB_NY_j$ Lewis pairs involve a key orbital interaction between the filled out-of-phase mixing of $N_3$ $2p_y$ and halogens $n_p$ orbitals of $N_j$, with the empty $B_3p_z$ orbital of BH$_3$, the HOMO(base)–LUMO(acid) interaction (see Figure 7; additional stabilizing contribution from the HOMO-2(base)–LUMO(acid) interaction is given in Figure S4). However, this interaction is relatively less stabilizing compared to borane–ammonia. As the $Y$ ligands vary from $H$ to the increasingly more electronegative atoms $I$, $Br$, $Cl$ and $F$, the HOMO drops in energy, which leads to a larger HOMO–LUMO energy gap ($\Delta E_{\text{HOMO–LUMO}} = 2.5$, $2.8$, $3.4$, $3.8$, and $5.5$ eV along $N_3$, $NBr_3$, $NCl_3$, $NF_3$, and $NI_3$, respectively). The corresponding orbital overlap (HOMO–LUMO), on the other hand, decreases on descending group 17, i.e. it becomes less favorable. Because of the out-of-phase mixing of the $n_p$ orbitals, the amplitude of HOMO is larger on the less electronegative atom (either $N$ or $Y$). Thus, the amplitude on the nitrogen atom decreases along the series NF$_3$, NCl$_3$, NBr$_3$, and NI$_3$, which decreases the spatial overlap with the empty $2p_z$ orbital of BH$_3$. Therefore, the trend in $\Delta E_{\text{HOMO–LUMO}}$ overrules the trend in (HOMO–LUMO), determining the trend in orbital interaction energies and, eventually, in the stability of the $H_jB_NY_j$ Lewis pairs.

Conclusions

At variance with the current view, the strength of archetypical $X_jB_NY_j$ Lewis pair (where $X,Y = H$, $F$, $Cl$, $Br$, and $I$) bonds is not solely attributed to the strength of the stabilizing frontier molecular orbital interactions. The bonding mechanism involving boron trihalides, for example, is determined by the amount of energy required to deform the fragments, especially the Lewis acid, upon complexation. This follows from our detailed bonding analyses based on relativistic dispersion-corrected density functional theory at ZORA-BLYP-D3(BJ)/TZ2P.
Our activation strain and quantitative Kohn–Sham MO analyses reveal that the bonding energy of the series X,B–NH₃ is determined by the strain energy associated with the geometrical distortion of the Lewis acid on going from the planar to the pyramidal geometry acquired in the Lewis complex. We have, for the first time, quantitatively decomposed the strain energy of the Lewis acid in terms of the change in the interaction energy within one fragment upon its deformation. The decrease in the strain energy directly correlates with the weakening of the B–X bond as the electronegativity of X decreases along the series: F, Cl, Br, and I. Most of this effect arises from the bonding in the plane of the molecule, not in the π system as is widely believed. In other words, the less destabilizing energy required to deform a weak B–X bond results in a smaller strain energy, which manifests in a more stable Lewis pair. This is the actual reason why the Lewis pairs become systematically stronger as BXₓ goes from BF₃ to Blp and not because of a more stabilizing interaction energy as is the currently accepted rationale. For the H₃B–NY₃ series, the bonding is driven by the charge-transfer stemming from the commonly accepted HOMO–LUMO interaction between the lone pair on the nitrogen of the Lewis base and the empty p orbital at the boron of the Lewis acid.

This work clearly demonstrates the role of the strain energy, besides the well-known donor–acceptor orbital and also electrostatic interactions, in playing a leading role in determining the strength of Lewis acid/base interactions. Our findings are both chemically intuitive and grounded in quantum chemical findings based on state-of-the-art computations. Importantly, we have brought our understanding of these fundamental interactions into the 21st century and hope that this work will be useful for the development of novel Lewis pair chemistries.

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**Conflict of Interest**

The authors declare no conflict of interest.

**Keywords:** Activation strain analysis · Bond energy · Density functional calculations · Energy decomposition analysis · Lewis acid-base pairs

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