ABSTRACT: Detection of individual molecules is the ultimate goal of any chemical sensor. In the case of gas detection, such resolution has been achieved in advanced nanoscale electronic solid-state sensors, but it has not been possible so far in integrated photonic devices, where the weak light-molecule interaction is typically hidden by noise. Here, we demonstrate a scheme to generate ultrasensitive down-conversion four-wave-mixing (FWM) in a graphene bipolar-junction-transistor heterogeneous D-shaped fiber. In the communication band, the FWM conversion efficiency can change steeply when the graphene Fermi level approaches 0.4 eV. In this condition, we exploit our unique two-step optoelectronic heterodyne detection scheme, and we achieve real-time individual gas molecule detection in vacuum. Such combination of graphene strong nonlinearities, electrical tunability, and all-fiber integration paves the way toward the design of versatile high-performance graphene photonic devices.

KEYWORDS: graphene, four-wave mixing, fiber integrated optics, individual gas molecule detection

Graphene displays exceptionally strong light-matter interaction and gate-tunable nonlinear optical properties, ranging from difference frequency generation (DFG) based on second order nonlinearities to third-order harmonic generation (THG) and four wave mixing (FWM) based on third order nonlinearities, spurring applications such as optical parametric amplifiers, oscillators, switches, frequency converters, and detectors. Graphene gapless Dirac Fermions enable a unique broadband response that ranges from terahertz to ultraviolet. Moreover, thanks to the atomic flexibility of graphene and related van der Waals integration techniques, graphene can be easily deposited and tailored on-chip or on-fiber, thus further enhancing its potentials for integrated device applications. When transferred on waveguides and fibers, graphene gating can also be used to tune the device optical conductivity and thus to achieve phase matching. Here, we report electrically tunable frequency down-conversion in graphene heterogeneous silica D-shaped fiber (GhDF), driven by femtosecond degenerate FWM. In this device geometry, the graphene on-fiber is directly exposed to air, thus enabling molecule–graphene interactions and ultrasensitive gas sensing. When the graphene \( E_F \) is preset at \( \sim 0.4 \) eV and we use a pump wavelength of \( \sim 1560 \) nm, FWM in our GhDF device becomes extremely sensitive to molecular adsorption/desorption, enabling label-free individual molecule detection for \( \text{NH}_3 \) and \( \text{CO}_2 \) in vacuum environment.

Figure 1a shows a sketch of our GhDF device. The cladding fiber is directly exposed to air, thus enabling molecule–graphene interactions and ultrasensitive gas sensing.
Figure 1. Design and implementation of the GhDF for electrically tunable FWM. (a) Sketch of the FWM process. A graphene bipolar junction is fabricated on the side-polished fiber. (b) Top-view optical microscope image of the GhDF device. The graphene channel region is zoomed in, showing the Au–graphene–Au geometry. The bright left-to-right horizontal line is the D-shaped fiber. The scale bar is 50 μm. (c) Sectional view of the electric field distribution in the GhDF with fiber core diameter 6 μm. Scale bar, 10 μm. Here the yellow dashed line highlights the graphene monolayer, and the electric field is vertically polarized (TM polarization). (d) Electronic measurement of the graphene BJT. The kink in the $V_{SD}$–$I_{SD}$ curve at $V_{SD} = 11.5$ V indicates the position of the Dirac point. (e) Calculated (black dashed curve) and measured (orange curve and dots) increase in temperature when a source-drain voltage is applied to the GhDF. (f) Theoretically modeled refractive index as a function of the Fermi level based on the extracted chromatic dispersion of the device. Measured data points are shown in red dots. The error bar represents the measurement uncertainty estimated from the interferometric measurements under the same conditions.
energy conservation as the central wavelength of the continuous seed, the pulsed pump, and the generated Stokes line are 1548, 1561, and 1573 nm, respectively, allowing the FWM to be electrically tunable when we change the graphene Fermi level via tuning of \(V_{\text{SD}}\). When \(E_F\) increases from 0 to 0.47 eV, the Stokes power decreases gradually. (b) Measured Stokes power (blue dots) and the calculated graphene third-order nonlinear coefficient \(\chi^{(3)}\) versus the graphene Fermi level. Here the black dashed curve is the moving-average fitting of \(\chi^{(3)}\). (c) Measured beat note of the enhanced seed at 37.8 MHz. (d) The seed enhancement varies when tuning the \(\lambda_{\text{seed}}\) from 1500 to 1600 nm. When the detuning approaches 0, the FWM has the highest conversion efficiency.

Figure 2. Electrically tunable FWM in the graphene heterogeneous D-shaped fiber. (a) Measured spectrum, ranging from 1520 to 1590 nm. Here the central wavelength of the continuous seed, the pulsed pump, and the generated Stokes line are 1548, 1561, and 1573 nm, respectively, allowing energy conservation as \(2\lambda_{\text{Pump}} = \lambda_{\text{Seed}} + \lambda_{\text{Stokes}}\). The FWM is electrically tunable when we change the graphene Fermi level via tuning of \(V_{\text{SD}}\). When \(E_F\) increases from 0 to 0.47 eV, the Stokes power decreases gradually. (b) Measured Stokes power (blue dots) and the calculated graphene third-order nonlinear coefficient \(\chi^{(3)}\) versus the graphene Fermi level. Here the black dashed curve is the moving-average fitting of \(\chi^{(3)}\). (c) Measured beat note of the enhanced seed at 37.8 MHz. (d) The seed enhancement varies when tuning the \(\lambda_{\text{seed}}\) from 1500 to 1600 nm. When the detuning approaches 0, the FWM has the highest conversion efficiency.

Information Movie 1. The stabilized mode locked fiber laser launches a maximum average power of \(\sim 3\) mW into the GhDF, corresponding to a maximum peak power of \(\sim 0.3\) kW (37.8 MHz repetition, 265 fs pulse duration). Thus, for the 13 nm pump-seed detuning, the nonlinear conversion efficiency is \(\sim 55\) dB when \(E_F < 0.2\) eV, in agreement with recent results on FWM from graphene on waveguides.\(^{19,20}\) We notice that the observed modulation of the Stokes power with the external voltage (Figure 2b) is due to both multiphoton resonant transitions and tuning of the phase matching condition (a higher \(E_F\) induces a larger \(n_g\), resulting in a smaller nonlinear gain). Note that the multiphoton resonance does not occur exactly at \(\hbar\omega = 2E_F\), being \(\hbar\omega \approx 0.8\) eV for our pump wavelength (1560 nm). This is due to the effect of the high electronic temperature reached in nonlinear experiments and quantum interference between the multiphoton resonant transitions contributing to the FWM nonlinear optical susceptibility, as also observed in previous studies.\(^{9,20}\) Finally, we plot the calculated graphene \(\chi^{(3)}\) (red dots in Figure 2b). When \(E_F\) increases from 0 to 0.5 eV, the \(\chi^{(3)}\) of the GhDF is tuned from \(8 \times 10^{-17}\) to \(6 \times 10^{-18}\) m\(^2\)/V\(^2\), considering the transverse mode area in the fiber of \(\sim 40\) \(\mu\)m\(^2\).

Energy conversion in an FWM process can be tested either by measuring the pump depletion (\(\Delta P_{\text{Pump}}\)) or the seed enhancement (\(\Delta P_{\text{Seed}}\)), given the relation \(2\Delta P_{\text{Pump}} = \Delta P_{\text{Seed}} + P_{\text{Stokes}}\). We measure the self-beat of the FWM enhanced seed by using a balanced photodetector (Figure 2c). Without FWM,
the continuous wave seeding cannot have any beat note. On
the other hand, the FWM process transfers energy at a
fixed repetition rate of 37.8 MHz from the pulsed pump to the CW
seed. We thus observe oscillations (at 37.8 MHz rate) in the
seed enhancement on top of its DC average power, as shown
also in Supporting Information Figures S7 and S8. Measure-
ments of $\Delta P_{\text{Seed}}$ also enable us to identify the nonlinear
conversion efficiency as a function of the pump-seed detuning.
In order to test this, we fix the pump wavelength and scan the
seed wavelength from 1500 to 1600 nm while monitoring $\Delta P_{\text{Seed}}$ (Figure 2d). As expected from the phase matching
condition, larger detuning gives smaller nonlinear enhance-
ment. When $\lambda_{\text{Pump}} - \lambda_{\text{Seed}}$ approaches 0, we observe the
highest FWM conversion efficiency. At this point, we estimate $y \Re \chi^{(3)}$ of $\sim 10^{-15}$ m$^2$/V$^2$, in agreement with previous
studies.\textsuperscript{9,20}

The steep change in the FWM efficiency when the graphene
$E_F$ approaches 0.4 eV can be used as an ultrasensitive tool for
chemical sensing. Indeed, gas adsorption on graphene can modulate the $E_F$ via both charge transfer and impurity
doping\textsuperscript{5,24,34} and, as a consequence, it will affect $\Delta P_{\text{Seed}}$ during the FWM experiment. Figure 3a schematically shows
the case of NH$_3$ and CO$_2$ molecules attached to the GhDF. In
the limiting case of individual molecular interaction, NH$_3$ will
act as a donor material with two electrons per molecule, thus
directly affecting the graphene’s $E_F$.\textsuperscript{23,35} Moreover, we highlight
that since the sensing mechanism for NH$_3$ molecule is based
on the contribution of lone electron pairs from the N atom in
the NH$_3$ molecule, our sensing scheme could be used also for
the detection of other amino molecules (e.g., NH$_2$CH$_3$ and
N(CH$_2$CH$_3$)$_3$). On the other hand, CO$_2$ adsorbed on the
graphene introduces scattering impurities, thus changing the
refractive index of graphene.\textsuperscript{24} Figure 3b shows the
quantitative simulations of the nonlinear gain coefficient $\gamma$ of
the GhDF when changing the graphene’s $E_F$ and the GhDF’s
refractive index $n_i$ being $\gamma = n_i \omega_1 / (c A_{\text{eff}})$ and $n_i = 3 \pi n \Re \chi^{(3)} / 4 \epsilon_0 n^2 c^2 A_{\text{eff}}$ the nonlinear refractive index. In this equation, $n = 1.46$ is the (linear) refractive index of the GhDF (without adsorbed molecules), $f = 192.3$ THz is the optical frequency, $c$ is the speed of light in vacuum, $\epsilon_0$ is the vacuum permittivity, and $A_{\text{eff}} \approx 40 \mu$m$^2$ is the effective transverse mode area of the
GhDF. We thus obtain $\gamma \approx 1.135$ m$^{-1}$ W$^{-1}$. In this framework,
NH$_3$ adsorption increases the graphene Fermi level (and thus
affects mainly $\Re \chi^{(3)}$) while CO$_2$ adsorption decreases the

Figure 3. Mechanism and experimental setup for gas sensing. (a) Sketch of NH$_3$/CO$_2$ adsorption on graphene. The gas molecule adsorption
induces either charge transfer or structural impurity. (b) Simulation of the three-dimensional correlation: the Fermi level ($E_F$), the effective
refractive index of the GhDF ($n_i$), and the third order nonlinear coefficient ($\gamma$). NH$_3$ adsorption mainly changes the $E_F$, while CO$_2$ adsorption
mainly changes the $n$. Each NH$_3$/CO$_2$ molecular adsorption induces $\Delta P_{\text{Stokes}}$ of $\sim 9.44 \times 10^{-7}$ nW. (c) Experimental setup. The GhDF is fixed
in a temperature-controlled vacuum chamber. Here, BPD, balanced photodetector; OSA, optical spectrum analyzer; OSC, oscilloscope. (d)
Performance of the lock-in amplification with amplification of the modulated signal $>$60 dB. (Inset) The thermal feedback induced uncertainty is
$\pm 0.15$ mV with thermal noise frequency $\sim 1$ Hz.

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(linear) effective index ($n$) of the GhDF. Supposing that graphene is predoped around 0.4 eV, and the effective area of the device is $\sim 5 \times 10^{-10}$ m$^2$, then (i) single NH$_3$ molecule adsorption will decrease the carrier density by $4 \times 10^9$ m$^{-2}$, leading to an $E_F$ of $\sim 9.8 \times 10^{-9}$ eV per molecule. Here, we have used $E_F \approx \hbar v_F (\pi N)^{-1/2}$, where $v_F = 1 \times 10^6$ m/s is the Fermi velocity. Thus, based on the results shown in Figure 2b ($E_F$ versus $P_{\text{Stokes}}$ relation: $\approx -90$ nW/eV), in our device a single NH$_3$ molecule adsorption event will induce a reduction of the Stokes power of $\sim 9 \times 10^{-7}$ nW per molecule. (ii) Individual CO$_2$ molecule adsorption will increase the graphene resistance via impurity doping, thus reducing the effective refractive index by $10^{-12}$, estimated by using FET calculations. This leads to an increase of $\gamma$ of $\sim 2.4 \times 10^{-7}$ m$^{-1}$ W$^{-1}$. Thus, individual CO$_2$ molecule adsorption will increase the Stokes power by $\sim 4.4 \times 10^{-7}$ nW per molecule (see also Supporting Information Note S1). Since the expected changes in the Stokes power upon single molecule adsorption are considerably lower compared to our noise level of $\sim 0.1$ nW, in order to detect individual adsorption/desorption dynamics we performed heterodyne optoelectronic measurements in vacuum, as depicted in Figure 3c. Before launching into the GhDF, we use a 1:1 fiber coupler to mix the femtosecond pulsed pump and the continuous wave seed. The polarization of both is optimized independently. The GhDF is fixed in a vacuum chamber equipped with a 4-probe station, which is used for electrical tuning of the GhDF. The volume of the vacuum chamber is 8 L with maximum vacuity of $10^{-5}$ Torr. Inside the chamber, we use a thermoelectric cooler (TEC) to control the temperature with 10 mK accuracy. Since our single molecule detection is based on the precise measurement of $\Delta P_{\text{seed}}$ (i.e., we need to measure $\Delta P_{\text{seed}} \approx 10^{-7}$ nW), in our experiments we use a fiber Bragg grating based tunable filter (bandwidth 0.1 nm centered at 1547.84 nm to filter the seed wavelength) and balanced detection to remove the DC components. Afterward, we use a stable RF generator to beat the repetition frequency of $\Delta P_{\text{seed}}$ for further amplification and frequency down conversion. The two-step beating-based

Figure 4. Gas sensing performance. (a,b) Locked-in amplified voltage $\Delta P_{\text{seed}}$ when sensing NH$_3$ (blue curve) and CO$_2$ (red curve). The NH$_3$ adsorption decreases the FWM efficiency while CO$_2$ adsorption increases the FWM efficiency. When zooming-in the curves over tens of milliseconds, molecular on/off dynamics become evident. Here the gray curve shows the reference voltage when there is no gas molecule in the vacuum chamber (0 nM/L). (c) In the dynamically stable region, we count the molecular on/off (adsorption/desorption) events. The obtained statistics follow a power law, as discussed in the main text. (d,e) (Left) Gas concentration versus average measured voltage. The maximum macrosensitivity for NH$_3$ and CO$_2$ are $\sim 120$ and 15 mV/nM. (Right) By electrically tuning the graphene temperature, our device shows good recoverability.
heterodyne amplification finally boosts the minor signal alteration over >60 dB (Figure 3d). With such amplification (>6 orders of magnitude), we are able to detect \( \Delta P_{\text{seed}} \approx 10^{-7} \) nW. In other words, the heterodyne-based lock-in amplification technique is a powerful tool for weak signal extraction, which is uniquely suitable for nonlinear detection and high precision sensing.\(^5\) We note that such measurement is extremely sensitive to power fluctuations, thus we have to carefully stabilize the optical sources and the device temperature. In this regard, we apply a thermal feedback with response rate of 1 Hz. However, despite the applied stabilization we can still observe thermally induced fluctuations of ±0.15 V. Hence, in order to avoid cross-influence during gas sensing experiment, we carefully control the gas concentration with nM/L precision, making sure that the gas molecular on/off dynamics has a rate >100 Hz, much faster than the thermal fluctuation. Gas preparation is discussed in Supporting Information Note 2, and Supporting Information Figure S8 plots the spectral characterization and noise suppression of this optoelectronic heterodyne system.

Figure 4 shows the sensing capability of our GhDF device. Figure 4a shows the changes in the locked-in amplified signal \( \Delta P_{\text{seed}} \) upon an increment of the NH\(_3\) gas concentration from 0 to 40 nM/L, while Figure 4b shows the case of CO\(_2\) gas injection. As explained in Figure 3, the NH\(_3\) (CO\(_2\)) adsorption leads to a lower (higher) FWM efficiency. For an integration time of 10 μs, the maximum sensitivity of our GhDF is higher than 120 mV/nM for NH\(_3\) and 15 mV/nM for CO\(_2\) (left panel in Figure 4d). The uncertainty of our lock-in amplification based measurement is ±1 mV. In this vacuum environment, 1 nM means 0.6 molecules/μm\(^2\), and thus, considering the effective graphene–gas interaction area of our device of 500 μm\(^2\), there could be tens to hundreds of molecules adsorbed on the graphene surface simultaneously. Thus, in order to characterize the molecular dynamics, we zoom-in the time trace to detect individual molecule adsorption events (Figure 4a,b). Individual gas molecules attaching or detaching from the graphene will induce discrete steplike changes with integer common denominator on a < 10 ms time-scale (i.e., the inverse of our gas on/off rate >100 Hz). Experimental results (Figure 4a,b) show that in the case of NH\(_3\) the smallest voltage step is 4 mV, while for CO\(_2\) the smallest step is 2 mV. For the detection of the Stokes Power, we used an InGaAs balanced photodetector (Newport Nirvana 2017), which has a conversion gain of \( \sim 10^6 \) V/W at 1550 nm. Thus, considering the amplification due to lock-in detection of 66.2 dB (Figure 3), the measured electrical signal will be ~2 mV for individual CO\(_2\) molecules (4.4 × 10−7 nW) and ~4 mV for individual NH\(_3\) molecules (9 × 10−7 nW), in agreement with experimental results. Such discrete steps strongly point toward individual molecule adsorption/desorption events and demonstrate the individual molecule detection capability of our system. The NH\(_3\) on/off interval (\( \sim 5 \) ms per step) is significantly larger than the CO\(_2\) on/off interval (\( \sim 1 \) ms per step), because the NH\(_3\)–graphene bonding is tighter compared to CO\(_2\)–graphene, that is, the NH\(_3\) adsorption on graphene is more stable (see also Supporting Information Figure S9). Moreover, we counted the molecular on/off events (total number 1000, Figure 4c). We estimated the number of molecules that are adsorbed/desorbed on our device as the ratio between the observed steps (in mV) and the minimum step expected for individual molecule adsorption/desorption events, that is, 4 and 2 mV for NH\(_3\) and CO\(_2\) respectively. When the GhDF is exposed either to NH\(_3\) or to CO\(_2\), in the quasi-static state, large steps were rare (such as 10+ molecules on/off), whereas unit steps were dominant. These statistical results obey a power-law distribution, which is also a sign of individual molecule adsorption events.\(^23\) In particular, we can fit the molecules-counts correlation of NH\(_3\) and CO\(_2\) with the power-law \(1/N^{2.6}\) and \(1/N^{2.1}\), respectively. This result further suggests that, as previously discussed, adsorption on graphene is stronger in the case of NH\(_3\) compared to CO\(_2\). Additional measurements down to 10 pM/L concentration are shown in Supporting Information Figure S10. Finally, we note that adsorbed molecules can be efficiently released from the graphene surface by temperature-induced annealing. As shown in the right panel of Figure 4d, by tuning the device temperature between 300 and 370 K we achieve almost 100% recovery of the initial graphene properties for both NH\(_3\) and CO\(_2\). The recovery time constant is less than 1 min.

In summary, electrically tunable FWM was achieved in a graphene heterogeneous D-shaped fiber device. By changing the graphene Fermi level from 0 to 0.5 eV, the Re(\( \phi \)) of graphene can be modulated over 1 order of magnitude from \( 8 \times 10^{-17} \) to \( 8 \times 10^{-10} \) m\(^2\) V\(^{-2}\). A steep change (increase/decrease) of the FWM efficiency when the Fermi level approaches 0.4 eV allows for ultrasensitive characterization of third order nonlinearity of graphene. We exploit this feature to develop a fully integrated fiber-optic gas sensor device with gas molecule detection capability. As an application, the nonlinearity enhanced GhDF shows high performance as a label free and cheap fiber-optic sensor at room temperature with individual molecule sensitivity. Moreover, our integrated device, which combines graphene optical nonlinearity, electrical tunability, and on-fiber integration, will pave the way for other integrated photonic applications ranging from parametric amplification, photonic switching, frequency modulation, and high precision measurement.

**ASSOCIATED CONTENT**

*Supporting Information*

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.nanolett.0c02174.

- (S1) Electrically tunable four-wave-mixing in the graphene based D-shaped fiber; (S2) fabrication and characterization of the GhDF and device/setup preparation for sensing; (S3) measurements calibration and low concentration measurements; additional references and figures (PDF)

**FWM gate tunability (MP4)**

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