Optimal Scheduling of Multiple Sensors with Packet Length Constraint

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Abstract: This paper considers the problem of sensory data scheduling of multiple processes. There are \( n \) independent linear time-invariant processes and a remote estimator monitoring all the processes. Each process is measured by a sensor, which sends its local state estimate to the remote estimator. The sizes of the packets are different due to different dimensions of each process, and thus it may take different lengths of time steps for the sensors to send their data. Because of bandwidth limitation, only a portion of all the sensors are allowed to transmit in each time step. Our goal is to minimize the average of estimation error covariance of the whole system at the remote estimator. The problem is formulated as a Markov decision process (MDP) with average cost over an infinite time horizon. We prove the existence of a deterministic and stationary policy for the problem. We also find that the optimal policy has a consistent behavior and threshold type structure. A numerical example is provided to illustrate our main results.

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1. INTRODUCTION

Wireless sensor networks are nowadays ubiquitous in various fields, e.g., industrial automation, habitat monitoring, smart grid and autonomous traffic management (Akyildiz et al., 2002). In typical settings, after taking local measurements, the sensors send their data to a remote estimator through a wireless channel according to a protocol. The wireless connection saves wiring and enables remote operation. The channel capacity of wireless communication, however, is often limited. What is more, the wireless sensor nodes are usually battery powered. In order to tradeoff the estimation quality and limited available resources, e.g., bandwidth and energy, it is critical to wisely allocate resources for the sensors.

To deal with the scheduling problem in the wireless sensor networks, researchers considered the constraints on the channel bandwidth, energy budget, etc. To maximize lifetime of the network, Chamani and Pierre (2007) studied a policy switching between active and inactive modes. Performance optimization under energy budget constraint has also been investigated. Shi et al. (2011) considered optimal sensor data scheduling problem for a single sensor under a limited energy budget. The authors proved the optimality of a periodic scheduling policy. In Wu et al. (2013), an event-triggered transmission strategy was adopted to reduce the communication rate so as to save energy. In some applications, the sensors can interfere with each other, thus only a few sensors are allowed to be activated in each time slot. The sensor selection problem in this setting is considered, for example, in Gupta et al. (2006). Meanwhile, because of bandwidth limitation of communication channel, only a limited number of devices can transmit data at the same time. Optimal scheduling under channel bandwidth constraint was studied in Zhao et al. (2014), Mo et al. (2014), Hovareshti et al. (2007) and Han et al. (2017). Zhao et al. (2014) and Mo et al. (2014) considered scheduling over an infinite horizon and proved that the optimal scheduling scheme can be approximated arbitrarily by a periodic schedule. Hovareshti et al. (2007) showed that the estimation quality can be improved for smart sensors equipped with some memory and processing capacities. Han et al. (2017) proved that the optimal scheduling policy over an infinite horizon can also be arbitrarily approximated by a periodic schedule for the smart sensor case.

The previous works assumed that it take the same time for transmission of packets in different processes. The transmission of one packet is assumed to be done in one time step. However, the scales of processes vary and the packets transmitted by different sensors may also be different. In typical communication protocols, e.g., Time Slotted Channel Hopping (TSCCH, IEEE 802.15.4e), the transmission duration of different packets can be different and the data transmission scheme can be designed by the engineers. In Palattella et al. (2013), it was shown that...
TSCH protocol has superior energy efficiency compared with traditional IEEE802.15.4/ZigBee approaches. Standards of TSCH application can be found in Watteye et al. (2015).

Different from previous studies, our work focuses on the constraint of packet length. We study the sensor scheduling for remote state estimation of multiple LTI processes, each driven by white Gaussian noises, over an infinite horizon. Each process is measured by a sensor, which computes the local estimate of the process and sends the local estimate to a remote estimator. As the packet length of each process may be different, it costs different time duration for each sensor to complete one transmission of an estimate. Moreover, wireless sensor network has a bandwidth limitation: only a portion of all the sensor are allowed to transmit data to the remote estimator in one time step. We are interested in minimizing the average estimation error covariance of the remote estimator in this system. Our contributions are twofold.

1) We formulate the optimal scheduling of sensors under the packet length and bandwidth constraint as an average cost over an infinite time horizon Markov decision process. We prove that there exists a deterministic and stationary optimal policy by showing that the state space of Markov chain under optimal policy is finite.

2) By adopting dynamic programming, we prove that the optimal policy has a nice structure, i.e., consistency and threshold type structure. The consistency means that once a sensor is chosen to schedule, the transmission of the current estimate should not be interrupted by selecting another sensor. The threshold structure reduces searching space for off-line solution and facilitates online implementation.

The remainder of this paper is organized as follows. In Section 2, we develop the mathematical formulation of the problem of interest. The main results, which consist of the MDP formulation, the existence of a deterministic and stationary policy, and the consistency and the threshold structure of the policy, are given in Section 3. In Section 4, a numerical example is provided to illustrate the main results. We summarize the paper in Section 5.

Notation: Denote $\mathbb{N}$ as the set of nonnegative integer numbers. For a matrix $X$, let $\text{Tr}(X)$, $X^T$ and $\rho(X)$ represent the trace, the transpose and the spectral radius of $X$, respectively. The identity matrix is $I$, and its size is determined from the context. Let $P(\cdot)$ and $P(\cdot|\cdot)$ stand for the probability and conditional probability for certain events. Denote $\mathbb{E}[\cdot]$ as the expectation of a random variable.

2. SYSTEM SETUP AND PROBLEM FORMULATION

Consider the following $n$ independent discrete-time linear dynamic processes measured by $n$ sensors:

$$
x_k^{(i)} = A_k x_k^{(i)} + w_k^{(i)},
$$
$$
y_k^{(i)} = C_k y_k^{(i)} + v_k^{(i)},
$$
where $i \in \mathbb{N} \triangleq \{1, \ldots, n\}$, $x_k^{(i)} \in \mathbb{R}^{n_i}$ is the state of the $i$-th process at time $k$ and $y_k^{(i)} \in \mathbb{R}^{m_i}$ is the measurement at time $k$. The state disturbance noise $w_k^{(i)}$’s and the measurement noise $v_k^{(i)}$’s and the initial state $x_0^{(i)}$’s of each process are mutually independent Gaussian random variables with distribution $\mathcal{N}(0, Q_i)$, $\mathcal{N}(0, R_i)$ and $\mathcal{N}(0, P_i)$, respectively. We assume that $Q_i$’s and $P_i$’s are positive semidefinite, and $R_i$’s are positive definite. In this work, we consider the case when all the processes are unstable.

The sensors are assumed to have sufficient computation capacity. After obtaining the measurement $y_k^{(i)}$, the sensors calculate the local minimum mean square error (MMSE) estimate of $x_k^{(i)}$ using a Kalman filter:

$$
\hat{x}_{local,k}^{(i)} = A_k \hat{x}_{local,k-1}^{(i)},
$$
$$
P_{local,k}^{(i)} = A_k \hat{x}_{local,k}^{(i)} + Q_i,
$$
$$
K_{local,k}^{(i)} = P_{local,k}^{(i)} C_k^T (C_k P_{local,k}^{(i)} C_k^T + R_i)^{-1},
$$
$$
\hat{x}_{local,k}^{(i)} = \hat{x}_{local,k}^{(i)} + K_{local,k}^{(i)} (y_k^{(i)} - C_k \hat{x}_{local,k}^{(i)}),
$$
$$
P_{local,k}^{(i)} = (I_n - K_{local,k}^{(i)} C_k) P_{local,k}^{(i)} - K_{local,k}^{(i)} C_k P_{local,k}^{(i)} C_k^T K_{local,k}^{(i)},
$$
where $P_{local,k}^{(i)}$ stands for the a prior estimation error covariance, $P_{local,k}^{(i)}$ stands for the a posterior estimation error covariance, and $K_{local,k}^{(i)}$ is the optimal gain. The iteration starts with $\hat{x}_{local,0}^{(i)} = 0$ and $P_{local,0}^{(i)} = \Pi$. Since we assume that the initial error covariance matrix $P_{local,k}$’s are positive semidefinite, $(A_i, \sqrt{Q})$ is stabilizable and $(A_i, C_i)$ is detectable for each process, the above iteration of the a posterior estimation covariance $P_{local,k}^{(i)}$ converges exponentially fast to a steady state $P^{(i)}$ (Anderson and Moore, 1979). Without loss of generality, the local estimation covariances are assumed to enter the steady state in our problem.

Because the communication bandwidth is limited, at each time step, only $m$ out of the $n$ sensors are allowed to send their local estimates, $\hat{x}_{local,k}^{(i)}$ to the remote estimator. Let $\gamma_k^{(i)} \in \{0, 1\}$ denote whether the $i$-th sensor transmits its estimate at time $k$, i.e., if $\hat{x}_{local,k}^{(i)}$ is sent to the remote estimator, $\gamma_k^{(i)} = 1$; otherwise, $\gamma_k^{(i)} = 0$. Denote $\theta = \{\gamma_k^{(i)} : i = 1, 2, \ldots, n; k = 0, 1, 2, \ldots\}$ as the scheduling policy which specifies the value of $\gamma_k^{(i)}$ for each sensor at each time step.

Furthermore, as the sizes, $n_i$, of each dynamic process are different, the packet lengths of local estimate to be transmitted are also different. In some applications, e.g., underwater vehicles, the data rates are relatively low (Cui et al., 2006), and the local estimate is thus required to be split into more than one packet. The remote estimator needs all the relevant packets to decode the transmitted local estimate, $\hat{x}_{local,k}^{(i)}$. The local estimate of a higher dimension state may be split into more pieces than a lower dimension process. As a result, it may takes more time steps to transmit the whole packet for the higher

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1 The structural results for stable processes can also be obtained in the MDP framework, but the proofs are more lengthy. We consider the unstable processes for brevity.
dimensional process. Let $d_i$ denote the total time steps for the $i$-th process to transmit its local estimate. For example, suppose there are two processes. One of them is a scalar process whose dimension is 1, while the dimension of the other is 2. Suppose $d_1 = 1$ and $d_2 = 2$, then it takes 1 time step for the first process to transmit its local estimate, and 2 time steps for the second one.

For sensor $i$ at time $k$, denote $\hat{\eta}_{k,t}^{(i)} = 1$ for the arrival of $\hat{x}_{i,\text{local}}^{(i)}$ and $\hat{\eta}_{k,t}^{(i)} = 0$ otherwise. Define the time duration of missing local estimate at the remote estimator for the $i$-th sensor at time $k$ as

$$\tau_k^{(i)} = k - \max\{\ell : \hat{\eta}_{\ell,t}^{(i)} = 1\}. \quad (1)$$

Based on above settings, the remote estimator updates its remote estimation as follows:

$$\hat{x}_k^{(i)} = \begin{cases} A_{i,k}^{\tau_k^{(i)}} \hat{x}_{\text{local},k-\tau_k^{(i)}}^{(i)}, & \text{if } \hat{\eta}_{k,t}^{(i)} = 1, \\ A_{i,k} \hat{x}_{k-1}^{(i)}, & \text{if } \hat{\eta}_{k,t}^{(i)} = 0. \end{cases} \quad \text{(Lemma 3.1 in Shi and Zhang (2012))}$$

As the local error covariance is assumed to have entered the steady state, the estimation covariance matrices at the remote estimator are as follows:

$$P_k^{(i)} = \begin{cases} h_k^{(i)}(P^{(i)})^{(1)}, & \text{if } \gamma_k^{(i)} = 1, \\ h_k(P_k^{(i)-1}), & \text{if } \gamma_k^{(i)} = 0, \end{cases}$$

where the affine mapping of symmetric matrices $h_k(\cdot)$ and $h_k(\cdot)$ are defined as

$$h_k(X) \triangleq X, \quad h_k(X) \triangleq h_k \circ h_k \circ \cdots \circ h_k(X),$$

$$h_k(X) \triangleq A_k X A_k^T + Q,$$

where $\circ$ denotes function composition. The following properties of $h_k(\cdot)$ will be useful in later sections.

**Lemma 2.1.** (Lemma 3.1 in Shi and Zhang (2012)) The Lyapunov-like operator $h_k(X)$ is monotonic with respect to $\ell$, i.e., $\forall \ell \in N$, if $\ell_1 \leq \ell_2$ then $\ell_1 \leq \ell_2 \in \mathbb{Z}_+$, $h_k^{(i)}(P^{(i)}) \leq h_k^{(i)}(P^{(i)})$. Consequently, $\forall \ell \in \mathbb{Z}_+$, $\text{Tr}(P_k^{(i)}) < \text{Tr}(h_k(P_k^{(i)})) < \cdots < \text{Tr}(h_k^{(i)}(P^{(i)}))$.

The average per-stage cost of a scheduling policy is given as

$$J(\tau_0^{(1)}, \ldots, \tau_0^{(n)}, \theta) \triangleq \limsup_{T \to \infty} \frac{1}{T} \sum_{k=0}^{T-1} \sum_{i=1}^{n} \text{Tr}(P_k^{(i)}).$$

Note that the expectation is introduced because the scheduling policy might be random although the packet arrival is deterministic. With the above definition, the optimal scheduling policy is a feasible policy minimizing the total cost $J(\theta)$.

**Problem 2.2.**

$$\min_{\theta} J(\tau_0^{(1)}, \ldots, \tau_0^{(n)}, \theta) \quad \text{s.t.} \quad \sum_{i=1}^{n} \tau_k^{(i)} = m, \forall k \geq 0.$$

3. MAIN RESULTS

In this section, we solve Problem 2.2 by formulating it as an infinite time horizon Markov decision process with average cost criterion. First, we find that, without loss of any performance, the optimal scheduling policy can be restricted to be deterministic and stationary (independent of time index $k$). Furthermore, we show that the optimal policy is consistent and there is a threshold structure in the optimal policy.

3.1 MDP Formulation

For brevity, we assume $n = 2$ and $m = 1$ in the following discussion. We remark in Remark 3.7 that the structural results can be extended to general $n$ and $m$.

We formulate the Problem 2.2 as a discrete time MDP with a quadruplet $(S, A, P(\cdot|\cdot, \cdot), c(\cdot, \cdot))$. Each item above is explained as follows.

1) The state space $S$ consists possible states, which are defined as $s \triangleq (\tau_1, \tau_2, \nu_1, \nu_2) \in \mathbb{N}^4$. The estimate holding time $\tau_1$ and $\tau_2$ are short notations for $\tau_k^{(i)}$ defined in (1), where the time index $k$ is omitted for brevity. The remaining packets counter $1 \leq \nu_1 \leq d_1$ indicates how many packets are left to be sent to complete the transmission of the estimate of the $i$-th sensor. For example, suppose the estimate of sensor 1 consists of three packets and $\nu_1 = 2$ means that the first packet has been transmitted and there are still two packets to be transmitted.

2) The action $a$ is in the action space $A \triangleq \{1, 2\}$, where $a = 1$ or 2 means that the first or the second sensor is scheduled, respectively. Note that the available action can be a random policy on $a = 1$ and $a = 2$ which also meets the constraint in Problem 2.2.

3) The state transition, $P(s'|s, a)$, defines how the state transits from $s$ to $s'$ under action $a$. Because the channel is not lossy, the state transition under an action is deterministic. We state the state transition law as follows.

Given $s = (\tau_1, \tau_2, \nu_1, \nu_2)$ and $a = 1$, the next state is $s' = (1, \tau_2 + 1, 1, 1)$, if $d_1 = 1$

$$(1, \tau_2 + 1, 1, 1), \quad (1)$$

$$(\tau_1 + 1, \tau_2 + 1, \nu_1 - 1, d_2), \quad \text{if } d_1 > 1 \text{ and } \nu_1 - 1 > 0,$$

$$(d_1, \tau_2 + 1, d_1, d_2), \quad \text{if } d_1 > 1 \text{ and } \nu_1 - 1 = 0. \quad (2)$$

The state transition from $s$ under $a = 2$ is similar and omitted here.

4) The one-stage cost only depends on the current state and is defined as

$$c(s, a) \triangleq \text{Tr}(h_1^{(1)}(P^{(1)})) + \text{Tr}(h_2^{(2)}(P^{(2)})).$$

Let $H_k = (s_0, a_0, \ldots, s_{k-1}, a_{k-1}, s_k)$ be the history up to time $k$. A policy is a sequence $\{\pi_k\}_{k=0}^{\infty}$, where $\pi_k$’s are stochastic kernels from $H_k$ to $A$. Denote $\Pi$ as the set of all such feasible policies. Define the average cost associated with an initial state $s_0$ and a policy $a_k = \pi_k(H_k)$ by

$$J(s_0, \{\pi_k\}_{k=0}^{\infty}) \triangleq \limsup_{T \to \infty} \frac{1}{T} \sum_{k=0}^{T-1} \sum_{i=1}^{n} c(s_k, \pi_k(s_k)),$$

One may see that the Problem 2.2 is equivalent to the following problem.

**Problem 3.1.** Find the optimal policy $\{\pi^*_k\}_{k=0}^{\infty} \in \Pi$ such that
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The total cost of an optimal scheduling policy is a feasible policy minimizing the expected cost over a finite time horizon. The optimal policy is consistent and there is a threshold structure in the decision making process. We formally state the result in the following theorem.

**Theorem 3.3.** There exists a constant \( r^* \), a continuous function \( V(\cdot) \) on \( S \) and a deterministic and stationary policy \( \pi^* \in \Pi^{DS} \) that satisfies the following AOE

\[
\rho^* + V(s) = \min_{\pi \in \Pi^{DS}} \left[ c(s, \pi(s)) + E^s_\pi[V] \right],
\]

where \( E^s_\pi[V] \) is the conditional expectation of the value of the next state under policy \( \pi \), i.e., \( E^s_\pi[V] = \sum_{s' \in S} P(s'|s, \pi) V(s') \).

**Proof:** The results follows from Theorem 8.4.3 in Puterman (1994) as the state space and the action space are finite, the model is unichain and the cost is bounded.

**Theorem 3.4.** Consistency. If \( \alpha_k^* = \pi^*(s) = i \) and \( \nu_i \neq 1 \), \( i = 1, 2 \), then \( \alpha_{k+1}^* = i \), where \( \alpha_{k+1}^* = i \) denotes \( \alpha_{k+1}^* = \alpha_{k+2}^* = \cdots = \alpha_{k+n}^* = i \).

**Proof:** The proof can be found in the online version (Wu et al., 2016).

**Remark 3.5.** Theorem 3.4 agrees with intuition. Theorem 3.4 states that once one chooses to schedule one sensor, he should not abort the scheduling halfway, i.e., he should wait for the completion of transmission of the whole estimate before choosing another sensor to schedule again. In other words, when the last transmission is done, the scheduler chooses a sensor to schedule. The action should be consecutively executed until the packet has been fully delivered.

Now we present the threshold type policy of the MDP. The structural result will simplify off-line computation and facilitate online application of the scheduling policy. Note that we only consider the case when \( \nu_1 = d_1 = 2 \) and \( \nu_2 = d_2 = 3 \). As it is proved that the scheduling policy should be consistent, the decision of which sensor to schedule is only made when the packet(s) of one local estimate has(laves) been fully transmitted.

**Theorem 3.6.** Threshold type policy.

1. If \( \pi^*((r_1, r_2, d_1, d_2)) = 1 \), then \( \pi^*((r_1+z, r_2, d_1, d_2)) = 1 \), where \( z \) is any positive integer;
2. If \( \pi^*((r_1, r_2, d_1, d_2)) = 2 \), then \( \pi^*((r_1, r_2+z, d_1, d_2)) = 2 \), where \( z \) is any positive integer.

**Proof:** The proof can be found in the online version (Wu et al., 2016).

**Remark 3.7.** The threshold structure can be extended to general \( m \) and \( n \). Let \( \nu_i = 1, \forall i \in [1, n] \). For \( 1 \leq i \leq n \), define \( \tau_i^- = (\tau_1, \tau_2, \ldots, \tau_{i-1}, \tau_{i+1}, \ldots, \tau_n) \) as the state of the system except for the \( i \)-th process. There exists measurable functions \( \phi_i : N^n \rightarrow N \) and the optimal policy is as follows:

1. Choose the \( i \)-th sensor if \( \phi_i(\tau_i^-) \leq \tau_i \);
2. Don’t choose the \( i \)-th sensor if \( \phi_i(\tau_i^-) > \tau_i \).

The threshold policy has valuable properties because only the state on the boundary should be stored for implement-
4. NUMERICAL EXAMPLES

In this section, we present a numerical example to illustrate our theoretical results, namely the consistency (Theorem 3.4) and the threshold policy (Theorem 3.6).

Let $n = 2$ and $m = 1$ and the parameters of the two processes be as follows

$$A_1 = 1.4, \quad C_1 = 1, \quad Q_1 = 1, \quad R_1 = 1;$$

$$A_2 = \begin{bmatrix} 1.2 & 1 \\ 0 & 1 \end{bmatrix}, \quad C_2 = [1 0], \quad Q_2 = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \quad R_2 = 1.$$  

Moreover, the packet length of the first process is 3, while the second 4. It can be seen that the spectral radius are $\rho(A_1) = 1.4$ and $\rho(A_2) = 1.2$, respectively. By solving the corresponding Riccati equations, the steady state error covariance matrices at the sensor side are

$$\overline{P}^{(1)} = 0.70, \overline{P}^{(2)} = \begin{bmatrix} 0.84 & 0.40 \\ 0.40 & 2.00 \end{bmatrix}.$$  

Since the state space is countably infinite, we truncate the states space with finite states, which is similar to Ren et al. (2016). We use the MDP toolbox (Chadès et al., 2009) to calculate the optimal policy through the value iteration algorithm.

Fig. 2 illustrates the consistency of optimal policy in Theorem 3.4. According to the result of value iteration, sensor 1 should be scheduled at $(6, 6, 3, 4)$. Because of consistency of the optimal policy, the transmission of the local estimate should not be interrupted. To complete the transmission, sensor 1 should continue its transmission at $(7, 7, 2, 4)$ and $(8, 8, 1, 4)$. Accordingly, the next states are $(7, 7, 2, 4), (8, 8, 1, 4)$ and $(2, 9, 3, 4)$ in order. Fig. 2 presents the value of the possible ‘next’ state if either sensor 1 or 2 is chosen to schedule. The figure shows that scheduling sensor 1 always cause the value of next state to be less than scheduling sensor 2.

The threshold policy is presented in Fig. 3. It is clear that there is a decision boundary on the plane. Note that at state $(6, 6, 3, 4)$, it is optimal to schedule sensor 1. Following from the threshold policy, it is also optimal to schedule sensor 1 for $(x, 6, 3, 4), x \geq 6$. By fixing $\tau_2 = 6, \tau_1 = \tau_2 = 1$. Fig. 4 shows the value of the next state of the system if either sensor 1 or 2 is scheduled. We can observe that scheduling sensor 1 always yields the next state less valuable.

5. CONCLUSION

This paper has considered sensor scheduling problem in a time-slotted setting. Depending on the size of the packet to be transmitted, different time slots are allocated to different sensors. We have studied the problem of minimizing the average estimation covariance under the constraints on packet length and bandwidth, and have formulated it as an infinite time horizon Markov decision process with average cost criterion. We have found that there is a deterministic and stationary policy for the problem. Furthermore, we have shown that the optimal policy has consistency and threshold structures. The consistent behavior means that once a sensor is chosen to schedule, the transmission of current estimate should not be interrupted. The threshold type structure has reduced searching space and has facil-
ate online implementation. A numerical example has been provided to illustrate our results.

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