Demonstration of relativistic electron beam focusing by a laser-plasma lens

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Laser-plasma technology promises a drastic reduction of the size of high-energy electron accelerators. It could make free-electron lasers available to a broad scientific community and push further the limits of electron accelerators for high-energy physics. Furthermore, the unique femtosecond nature of the source makes it a promising tool for the study of ultrafast phenomena. However, applications are hindered by the lack of suitable lens to transport this kind of high-current electron beams mainly due to their divergence. Here we show that this issue can be solved by using a laser-plasma lens in which the field gradients are five order of magnitude larger than in conventional optics. We demonstrate a reduction of the divergence by nearly a factor of three, which should allow for an efficient coupling of the beam with a conventional beam transport line.
Elelectron beams from laser-plasma accelerators\textsuperscript{1–3} have typical normalized transverse emittances of about or below 1 mm mrad (refs 4–7), comparable or even smaller than those of linear accelerators delivering similar energies\textsuperscript{8,9}. Yet, this small emittance is mostly due to a sub-micrometer source size\textsuperscript{10}, while the beams typically have rather large divergence of a few milliradians. Their energy spread, of a couple of per cents\textsuperscript{11}, is also at least one order of magnitude larger than in linear accelerators. This raises several issues for the beam transport and hence for key applications of laser-plasma accelerators such as free-electron lasers and high-energy colliders\textsuperscript{12–15}. In particular, the transverse emittance tends to increase during a free drift because electrons with different energies rotate with different velocities in the transverse phase space\textsuperscript{16}. The emittance increase is tolerable\textsuperscript{17} if the drift length \( L \leq \left( \frac{\gamma_0 E_0}{\sigma_E} \right) \). Here \( \gamma_0 \) is the initial normalized emittance, \( \gamma_0 \) is the mean Lorentz factor, \( E_0 \) is the root mean square (r.m.s.) relative energy spread and \( \sigma_E \) is the r.m.s. divergence. Regarding state of the art laser-plasma accelerators\textsuperscript{5,7,11,18}, the above condition indicates that the drift length should be smaller than 1–5 cm, depending on the exact conditions. In other words, electrons must be focused within a few centimeters from the accelerator exit in order to be transported efficiently.

Focusing the beam within such a short distance requires very high transverse field gradients. Quadrupole magnets, which are generally used to transport electron beams, operate at gradients of \( \sim 50 \text{T m}^{-1} \), which is two orders of magnitude less than required. Although using non-adjustable permanent magnet configurations with millimetre-size aperture, field gradients of up to \( 500 \text{T m}^{-1} \) have been reported\textsuperscript{19}, further enhancement is limited due to manufacturing issues, demagnetization effects and so on. An electron beam transport line based on quadrupole technology will therefore degrade the quality of a laser-plasma electron beam, rendering it useless for most applications. As they can sustain much higher gradients, plasmas could help to drastically miniaturize focusing optics, similar to the miniaturization achieved by laser-plasma accelerators, and hence to avoid any emittance growth. Incidentally, the idea to use plasma to focus an electron beam\textsuperscript{20} is almost as old as the idea to use plasma to accelerate electrons\textsuperscript{21}. It was proposed to focus an electron beam using the radial fields created in the wake of the electron beam itself, when it propagates in a plasma. The so-called plasma lens was demonstrated in the context of conventional accelerators\textsuperscript{22–25}, but it has not been considered for focusing electron beams from laser-plasma accelerators owing to the ultrashort length of these beams. Indeed, there is always a finite length at the bunch head over which the focusing is very non-uniform\textsuperscript{26,27}; for ultrashort bunches from laser-plasma accelerators this length is comparable to the bunch length\textsuperscript{28}. The laser-plasma lens was recently proposed, and validated by three-dimensional particle-in-cell simulations, to solve this issue\textsuperscript{29,30}.

In the following, we present an experimental demonstration of this concept. First, we explain the principle of the laser-plasma lens. Then, we show that the strength of the lens can be optimized by tuning both the distance between the accelerator and the lens, and the electron density in the lens. Finally, we analyse the chromaticity of the lens and discuss the results.

**Results**

**Principle of the laser-plasma lens.** In a laser-plasma accelerator, the wakefields in which electrons are accelerated present both longitudinal components, which are responsible for the energy gain\textsuperscript{23}, and transverse components, which make electrons oscillate and lead to betatron radiation\textsuperscript{24}. The idea of the laser-plasma lens is to use these transverse fields to focus the electron beam. Its principle is illustrated in Fig. 1a. A laser pulse drives a wakefield in a first gas jet, diffracts in free space, and drives again a wakefield in a second jet. As a result, an electron beam is generated and accelerated in the first jet, it then drifts in the free space, where the interaction with the plasma is negligible, and is focused by the transverse components of the wakefield in the second jet. In general, transverse oscillations in a laser wakefield cannot be used to focus an electron beam because the beam electrons oscillate out of phase (there is no correlation between the electron position and its propagation angle). In a laser-plasma lens, the required synchronization is operated by the free drift. During the drift, the trajectory of individual electrons is \( r(z) = r_0 + \theta_0 z \), with \( r_0 \) and \( \theta_0 \) being the transverse position and propagation angle, respectively, at the accelerator end, and \( z \) is the longitudinal distance from the accelerator end. Hence, for \( z \gg r_0 / \theta_0 \), \( r \) is almost proportional to \( \theta_0 \), the position is strongly correlated to the propagation angle. Because of this correlation, electrons oscillate almost in phase in the second laser wakefield (the laser-plasma lens), except for a small detuning arising from the beam energy spread (which impacts the oscillation frequency) and from the dependance of \( r \) on \( r_0 \). Thus, the plasma can act as a lens whose strength depends on its length and density. More specifically, the electron beam will be collimated if the focusing fields vanish when the transverse momentum is minimum for most electrons.

The principle of the laser-plasma lens is further illustrated by the phase-space traces in Fig. 1b. The free drift creates a correlation between \( r \) and \( \theta \), then the phase-space trace rotates in the second gas jet, leading to a decrease of the beam divergence. The trace area gives the transverse emittance, which is conserved.
during the focusing process. This emittance conservation can be used to estimate the minimum divergence \( \sigma_{\theta, \text{min}} \approx \varepsilon_N/(\gamma \sigma_0 L) \), where \( \varepsilon_N \) and \( \sigma_0 \) are the normalized emittance and the r.m.s. divergence at the accelerator end, respectively, and \( L \) is the distance between the two gas jets. We see that the drift length \( L \) is a key parameter to enhance the collimation. Note that this is a rough estimate, which assumes that the transverse fields in the lens are perfectly linear and neglects both the increase of the beam size during the phase-space rotation and chromatic effects, that is, influence of the beam energy spread; a more accurate analysis shows similar trends\(^29\). Note also that a noticeable electron density is tolerable in the drift space as long as the electron beam had a few pC charge and was stable shot-to-shot, confirming that electrons are injected into the accelerator by longitudinal self-injection\(^33\). The laser-plasma lens does not modify significantly the charge, the mean energy or the spectrum shape (Fig. 2a). In contrast, Fig. 2b shows that the beam divergence can strongly decrease in the lens, down to 1.6 mrad. The final divergence depends on the distance \( L \) from the accelerator to the lens. It decreases as \( L \) increases for \( L \gtrsim 1.8 \text{ mm} \) and increases with \( L \) for \( L \gtrsim 1.8 \text{ mm} \). The evolution of the divergence is governed by two effects, namely the decrease of the minimum achievable divergence \( \sigma_{\theta, \text{min}} \) and the decrease of the laser intensity, which reduces the strength of the focusing fields for long \( L \). Indeed, the Rayleigh length at the accelerator exit is \( \sim 400 \mu \text{m} \) (see Methods section). After 1.8 mm of propagation, the laser beam diameter and intensity are thus \( \Phi > 54 \mu \text{m} \text{ FWHM} \) and \( I < 8.3 \times 10^{17} \text{ W cm}^{-2} \). Therefore, the wakefield in the lens is in the linear regime and the strength of the focusing fields strongly depends on the laser beam size and intensity. More precisely, the gradient of the focusing fields in the lens evolves as \( (\gamma \sigma_0 L) \) as \( z \rightarrow 0 \). As a result, these fields can be too strong for short \( L \), leading to excessive focusing, and too low for long \( L \), leading to insufficient focusing. In Fig. 2, the transverse force seems to vanish for \( L \gtrsim 4.5 \text{ mm} \), while the lowest divergence is obtained for \( L \approx 1.8 \text{ mm} \). Note that for the shortest lengths, the wakefield may be in the nonlinear regime.

### Influence of the drift length

The laser-plasma lens, in the collimation configuration, was demonstrated at Laboratoire d’Optique Appliquée using the Salle Jaune laser system (see Methods section for information on the laser system, the gas targetetry and divergence measurements). The measured density profile is shown in Supplementary Fig. 1. At the end of the accelerator stage, electrons had a mean energy of \( \approx 241 \pm 12 \text{ MeV} \) (r.m.s. error) and a beam divergence of \( \approx 4.1 \pm 0.6 \text{ mrad} \). The electron beam had a few pC charge and was stable shot-to-shot, suggesting that electrons are injected into the accelerator by longitudinal self-injection\(^33\). The laser-plasma lens does not modify significantly the charge, the mean energy or the spectrum shape (Fig. 2a). In contrast, Fig. 2b shows that the beam divergence can strongly decrease in the lens, down to 1.6 mrad.

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### Influence of the plasma-lens density

In addition to the drift length, the electron density \( n_2 \) and the length of the second jet can also impact the lens properties. The influence of the electron density is illustrated in Fig. 3. According to the model from ref. 29, the focusing force varies as \( (k_0 \sigma_z \exp(-k_0^2 \sigma_z^2/2)) \sin(k_0 d) \), where \( k_0 \propto n_2^{1/2} \) is the plasma wave vector, \( \sigma_z \) is the r.m.s. length of the laser pulse and \( d \) is the distance between the laser and the considered electron. The term in brackets corresponds to the amplitude of the transverse wakefield, it is maximum when the laser pulse is resonant with the plasma wave, that is, for \( k_0 \sigma_z = 1 \). The strength of the lens depends also on the position of the electron beam in the wakefield. This effect is described by the sine

### Figure 2 | Influence on the electron beam divergence of the distance between the accelerator and the lens \( L \)

(a) Electron spectrum before and after the lens, normalized by \( 1.3 \times 10^2 \). The distance between the two stages is \( L = 1.8 \text{ mm} \). (b) FWHM beam divergence, at 270 MeV, as a function of \( L \). (c) Typical angularly resolved spectrum without laser-plasma lens. (d) Typical spectrum obtained for \( L = 1.8 \text{ mm} \). The colour scale indicates the number of electrons per MeV and mrad, divided by 17,000.

### Figure 3 | Influence on the electron beam divergence of the peak electron density in the second gas jet (the laser-plasma lens)

The divergence was measured for an electron energy of 270 MeV. The distance between the two stages is \( L = 2.3 \text{ mm} \). Data points were averaged over at least 11 shots; the vertical error bars correspond to the s.e.m. and the horizontal bar correspond to the precision on the backing pressure. The analysis of the interferograms leads to an additional systematic error on the density of \( \pm 5\% \).
plasma lens. The electron beam was accelerated in a laser-plasma
We demonstrated the collimation of an electron beam by a laser-
Discussion
enhances the focusing of low-energy electrons (similar results can
Fig. 3), the focusing fields are very weak and the divergence is
likely to occur only in the rising edge of the second gas jet (the
focus process is likely to occur only in the rising edge of the second gas jet (the
focusing force decreases as $z^{-2}$).

**Chromaticity of the lens**
Up to this point, the electron beam was implicitly assumed to be monoenergetic, and in Figs 2b and 3 only the divergence at 270 MeV was considered. Yet, a careful analysis of the angularly resolved electron spectra in Fig. 2c,d reveals that electrons of different energies are not focused to the same extend. This is shown more clearly in Fig. 4, which displays the reduction factor of the beam divergence as a function of both the electron energy and the distance between the two stages. A couple of observations can be made from this plot. First, the reduction factor is larger towards higher energies. This is likely due to the decrease of $\sigma_{0,\text{min}}$ at higher energies, both because $\sigma_{0,\text{min}}$ varies as $(\gamma \sigma_0)^{-1}$, and because in this particular experiment, the divergence $\sigma_0$ at the accelerator end increases with $\gamma$. Second, the optimal length $L$ decreases as the electron energy increases. This is because the amplitude of the transverse fields required to focus the beam increases with the electron energy. Lengthening $L$ tends to lessen the focusing fields and hence enhances the focusing of low-energy electrons (similar results can be obtained by decreasing the electron density). Nonetheless, Figs 2b,c and 4 show that an electron beam with an energy spread exceeding 100 MeV can be strongly focused, as a whole, using a laser-plasma lens.

**Methods**

**Laser system.** The experiment was conducted at Laboratoire d’Optique Appliquée with the ‘Salle Jaune’ Ti:Sa laser system, which delivers 0.9 Joule in the focal spot with a FWHM pulse duration of 26 fs and a linear polarization. The laser pulse was focused at the entrance of the first gas jet with a 1 m focal length off-axis parabola to a FWHM focal spot size of 12 \( \mu \)m. From the measured intensity distribution in the focal plane, the peak intensity was estimated to be $1.8 \times 10^{19}$ W cm$^{-2}$. The Rayleigh length in vacuum is \( \sim 400 \mu \)m. It is likely significantly shorter at the accelerator exit because of self-focusing.

**Gas targetry.** Helium gas jets were used for both the acceleration and the focusing stages. The two gas jets were produced by supersonic nozzles. The first has an exit diameter of 3 mm and a Mach number of 3, and the second has a diameter of 0.8 mm and a Mach number of 1.6. The laser was fired at 1.6 mm from the nozzle exits. The electron density profiles of both gas jets were characterized by interferometry and were analysed using the image processing programme Neutrino. The density profile in the acceleration stage had a plateau of 2.4 $\times$ 10$^{18}$ cm$^{-3}$. For even higher densities (not investigated in the experiment), the divergence should increase and eventually exceed the initial divergence when the fields become defocusing (for $k_d > \pi$). Note that, for long $L$, the mean density, which is effectively experienced by the electron beam during the focusing process, may be significantly smaller than the peak density indicated in Fig. 3, because the focusing process is likely to occur only in the rising edge of the second gas jet (the focusing force decreases as $z^{-2}$).

**Electron diagnostics.** The electron divergence was measured, in the vertical direction, from electron spectra. The electron spectrometer consisted of a permanent bending magnet (1.1 T over 10 cm), which deflects electrons depending on their energy, and a Lanex phosphor screen, which converts a fraction of the electron energy into 546 nm light imaged by a 16-bit visible CCD camera. The energy resolution varies between 1\% (for 140 MeV electrons with a beam divergence of 1\%$\theta_{rms}$) and 10\% (for 300 MeV electrons with a beam divergence of 4\%$\theta_{rms}$). The angular resolution is \( \sim 0.3 \) mrad. Two-dimensional footprints of the electron beam showed that the divergence is very similar in the horizontal and vertical directions. These footprints cannot be used to estimate the divergence reduction because of chromatic effects.

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**Author contributions**

C.T. proposed the experiment and wrote the paper with help from E.G., A.D. and R.L. E.G., A.D., C.T., K.T.P. and J.G. performed the experiment. E.G. analysed the results. R.L. and A.L. provided a theoretical support. A.L. realized Figure 1. J.-P.G. and A.T. designed, built and operated the upgraded laser system of Salle Jaune. A.F.T., S.S. and A.R. provided support for the operation of the facility. V.M. supervised the project.

**Additional information**

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