Impact of Channel Aging on Zero-Forcing Precoding in Cell-Free Massive MIMO Systems

Wei Jiang, Senior Member, IEEE, and Hans Dieter Schotten, Member, IEEE

Abstract—In the context of cell-free massive multi-input multi-output (mMIMO), zero-forcing precoding (ZFP) requires the exchange of instantaneous channel state information and precoded data symbols via a fronthaul network. It causes considerable propagation and processing delays, which degrade performance. This letter analyzes the impact of channel aging on the performance of ZFP in cell-free mMIMO. The aging effects of not only user mobility but also phase noise are considered. Numerical results in terms of per-user spectral efficiency are illustrated.

Index Terms—Cell-free massive MIMO, backhaul delay, channel aging, outdated CSI, phase noise, zero-forcing precoding.

I. INTRODUCTION

A s the latest advance of distributed massive multi-input multi-output (mMIMO) also known as network MIMO, a recent concept referred to as cell-free mMIMO has received much attention from academia and industry [1]. Applying a large number of transmit antennas makes linear precoding perform nearly as good as nonlinear precoding such as the optimal dirty-paper coding. Linear precoding is mainly implemented by conjugate beamforming (CB) or zero-forcing precoding (ZFP). The former is simple with low requirement on backhaul but suffers from inter-user interference. Consequently, many researchers focus on ZFP as well since it can achieve much higher spectral efficiency (SE), regardless of its higher implementation complexity and larger backhaul burden. The superiority of ZFP over CB in terms of spectral efficiency is demonstrated in [2], and its energy efficiency is analyzed in [3]. The uplink data throughput of ZFP under imperfect channel state information (CSI) is provided in [4] and its performance using quantized CSI is given in [5].

In cell-free mMIMO, ZFP requires the exchange of instantaneous CSI and precoded data between a central processing unit (CPU) and access points (APs) via a fronthaul network (also called backhaul in some literature, so both terms are interchangeable hereinafter). Masoumi and Emadi studied the system performance with limited backhaul capacity [6], while Buzzi et al. proposed a user-centric approach to lower the backhaul overhead [7]. However, these works only focus on the backhaul capacity but do not notice the effect of backhaul delay. In practice, the performance of ZFP is vulnerable to such a delay since the knowledge of CSI is outdated quickly under the channel fading and imperfect hardware, referred to as channel aging. The impact of channel aging has been extensively studied in different areas such as collocated mMIMO [8], [9], transmit antenna selection [10], coordinated multi-point transmission [11], and cooperative diversity [12], [13]. In cell-free mMIMO, [14] is the unique work until now but it only focuses on the effect of user mobility on the uplink rate. To the best knowledge of the authors, the downlink performance of cell-free mMIMO in the presence of channel aging is still missing. Meanwhile, the majority of the previous works only consider the Doppler shift raised by the relative mobility of users or surrounding reflectors, whereas the phase noise raised by imperfect oscillator is usually neglected [8]. The main contributions of this letter can be highlighted as follows:

- It is the first work to analyze the impact of channel aging on the performance of ZFP in distributed/cell-free mMIMO, and time alignment including all processing and propagation delays over the fronthaul network is modeled.
- A closed-form expression of SE, considering the effects of not only user mobility but also phase noise, is derived.
- In order to give some insights on the channel aging, representative numerical examples in terms of achievable per-user SE are illustrated.

II. SYSTEM MODEL

We focus on the downlink of a cell-free mMIMO system where M APs are randomly distributed over a geographical area. The APs are connected to a CPU via a fronthaul network and synchronized to serve K users, where \( K \ll M \), upon the same time-frequency resource. Each AP and user equipment (UE) is equipped with a single antenna. The downlink (DL) transmission from the APs to the UEs and the uplink (UL) from the UEs to the APs are separated by time-division duplex with the assumption of perfect channel reciprocity as [1], [2].

A. Channel Model

We adopt \( \sqrt{\beta_{mk} h_{mk}} \) to model the fading channel between AP \( m = 1, \ldots, M \) and UE \( k = 1, \ldots, K \), where \( \beta_{mk} \) and \( h_{mk} \) represent large-scale and small-scale fading, respectively. Small-scale fading is assumed to be frequency flat and is modelled by a circularly-symmetric complex Gaussian random variable with zero mean and unit variance, i.e., \( h_{mk} \sim CN(0, 1) \). Large-scale fading is frequency independent and keeps constant within a transmission block. It is given by \( \beta_{mk} = 10^{\frac{PL_{mk}}{10}} \).
with shadowing fading $X_{mk} \sim N(0, \sigma^2_{mk})$ and path loss $PL_{mk}$. As \[1\), the COST-Hata model is applied, i.e.,

$$PL_{mk} = \begin{cases} -L - 35 \log_{10}(d_{mk}), & d_{mk} > d_1 \\ -L - 10 \log_{10}(d_1^{1.5} d_{mk}^{0.5}), & d_0 < d_{mk} \leq d_1 \\ -L - 10 \log_{10}(d_1^{1.5} d_0^{0.5}), & d_{mk} \leq d_0 \end{cases}, \tag{1}$$

where $d_{mk}$ represents the distance between AP $m$ and UE $k$, $d_0$ and $d_1$ are the break points of the three-slope model, and

$$L = 46.3 + 33.9 \log_{10}(f_c) - 13.82 \log_{10}(h_{AP}) - [1.1 \log_{10}(f_c) - 0.7] h_{UE} + 1.56 \log_{10}(f_c) - 0.8$$

with carrier frequency $f_c$, the antenna height of AP $h_{AP}$, and the antenna height of UE $h_{UE}$.

**B. Channel Aging**

The performance of ZFP is affected heavily by the quality of instantaneous CSI \[4\], \[5\]. In cell-free mMIMO, there is a time gap between the instant when pilot sequences sound the UL channels and the instant of the DL data transmission due to the processing and propagation delays over the fronthaul network. Due to user mobility and phase noise, the acquired CSI may be outdated. This is called channel aging \[8\], \[9\], which may degrade the system performance substantially.

1) **User Mobility**: The relative movement between an AP and a UE as well as their surrounding reflectors leads to a time-varying channel. Given the moving speed $\nu_k$ of a typical UE $k$, its maximal Doppler shift is obtained by $f_d = \nu_k / \lambda$, where $\lambda$ represents the wavelength of carrier frequency. The higher the mobility, the faster the channel varies. To quantify the aging of CSI raised by the Doppler effect, a metric known as correlation coefficient is applied, as defined by \[13\]

$$\rho_k = \frac{\mathbb{E}[\hat{h}_{mk, d}^* h_{mk, p}]}{\sqrt{\mathbb{E}[|\hat{h}_{mk, d}|^2] \mathbb{E}[|h_{mk, p}|^2]}}, \tag{3}$$

where $\mathbb{E}[\cdot]$ stands for mathematical expectation, $h_{mk,p}$ and $h_{mk,d}$ denote the small-scale channel fading between AP $m$ and UE $k$ at the instants of the UL training (notated by $p$) and DL data transmission (notated by $d$), respectively. Under the classical Doppler spectrum of the Jakes model, it takes the value $\rho_k = J_0(2\pi f_d \Delta \tau)$, where $\Delta \tau$ stands for the overall delay, and $J_0(\cdot)$ denotes the zeroth order Bessel function of the first kind. According to \[12\], we have

$$h_{mk,d} = (\rho_k h_{mk,p} + e_{mk}) \sqrt{1 - \rho_k^2} \tag{4}$$

with an innovation component $e_{mk}$ that is a random variable with standard normal distribution $e_{mk} \sim N(0, 1)$.

2) **Phase Noise**: It is attractive for cost-efficient implementation of mMIMO systems with low-cost transceivers, but the problem of hardware impairments raises. Meanwhile, each distributed AP in cell-free mMIMO has to operate a local oscillator, in contrast to a common oscillator in a collocated mMIMO setup. Due to imperfect oscillators at the transmitter, the generated signals suffer from phase noise during the up-conversion from baseband to passband signals, and vice versa at the receiver \[8\]. Such phase noise is not only random but also time-varying \[15\], leading to the outdated CSI that is equivalent to that of user mobility. However, this effect is usually neglected in previous works such as \[9\], \[11\]–\[13\].

Utilizing a well-established Wiener process \[8\], \[16\], the phase noise of the $m^{th}$ AP and the $k^{th}$ UE at discrete-time instant $t$ can be modeled as

$$\begin{align*}
\phi_{mk,t} &= \phi_{mk,t-1} + \Delta \phi_t, \\
\varphi_{mk,t} &= \varphi_{mk,t-1} + \Delta \varphi_t, \quad \Delta \phi_t \sim CN(0, \sigma_\phi^2), \\
\Delta \varphi_t &= CN(0, \sigma_\varphi^2), \quad \sigma_\phi^2 = 4\sigma^2 f_c \tau_s, \quad i = \phi, \varphi \text{ with period } T_s \text{ and oscillator-dependent constant } c_i.
\end{align*} \tag{5}$$

where the increment variances are given by $\sigma_i^2 = 4\sigma^2 f_c \tau_s$, $\tau_s$ is the symbol period and $\phi, \varphi$ with symbol period $T_s$ and oscillator-dependent constant $c_i$. Then, we can write

$$g_{mk,t} = \sqrt{\beta_{mk}} h_{mk,d} e^{i(\phi_{mk,t} + \varphi_{mk,t})} \tag{6}$$

to denote the overall channel gain between AP $m$ and UE $k$ at instant $t$ combining the effects of path loss, shadowing, small-scale fading, and phase noise. In particular, the acquired CSI $g_{mk,p} = \sqrt{\beta_{mk}} h_{mk,p} e^{i(\phi_{mk,p} + \varphi_{mk,p})}$ is an outdated version of its actual value $g_{mk,d} = \sqrt{\beta_{mk}} h_{mk,d} e^{i(\phi_{mk,d} + \varphi_{mk,d})}$. Under good condition where the channels exhibit slow fading under low mobility and the quality of oscillators is high, the effect of channel aging is not explicit and the performance loss is possible to be small. Otherwise, the impact should be analyzed seriously.

**III. THE COMMUNICATIONS PROCESS**

This section introduces the communication process of a cell-free mMIMO system using zero-forcing precoding. A transmission block is divided into two phases: the UL training and DL data transmission, while the UL data transmission is neglected to focus on the DL performance analysis. Assume that the APs and the UEs are well-synchronized, and the knowledge of $\beta_{mk}$ is perfectly available. We also assume that the fronthaul network provides error-free and infinite capacity following the setup of previous works such as \[11\]–\[13\] so as to particularly focus on the backhaul delay. Hence, the discussion of practical backhaul constraints is out of scope for this letter and can refer to \[5\]–\[7\]. As illustrated in Fig. 1, the system operates as follows:
UEs transmit their pilot sequences $i_k, k = 1, \ldots, K$ with a duration of $T_p$. The propagation delay is $\tau_{sd}$.

- The $m^{th}$ AP, where $m = 1, \ldots, M$, can get the estimates $\hat{g}_{mk,p}, k = 1, \ldots, K$ with a processing time of $T_{ce}$.

- AP $m$ sends its local CSI $\bar{g}_m = \left[ \hat{g}_{m1,p}, \ldots, \hat{g}_{MK,p} \right]$ to the CPU, leading to a propagation delay of $T_{fb}$.

- Using $\hat{G} = [\hat{g}_1, \ldots, \hat{g}_M] \in \mathbb{C}^{K \times M}$, the CPU precodes the transmit symbols $s = [s_1, \ldots, s_K]^T$, where $E[|s_k|^2] = 1$.

- The time cost of the precoding is $\tau_f$. The CPU distributes the precoded symbol $\hat{s}_k = \hat{G} s_k$ to AP $m$, using the time of $T_p$.

- The transmitter of AP $m$ needs a preparation time of $\tau_{ix}$ to share the same sequence if $p_{mk} = p_{mk'}$.

- The pilot sequences be $\hat{s}_k$ to denote the set of indices for $\hat{g}_{mk,p}$.

- Let $\hat{g}_{mk,p}$ be the estimation error raised by additive noise and pilot contamination, we have

$$\hat{g}_{mk,p} = g_{mk,p} - \bar{g}_{mk,p}. \quad (9)$$

Other methods such as zero-forcing estimation can also be applied to acquire CSI, but it is independent with zero-forcing precoding discussed in this letter. The variance of $\hat{g}_{mk,p}$ is

$$E\left[ |\hat{g}_{mk,p}|^2 \right] = \frac{p_{mk}^2}{p_u \sum_k c_{pk} \beta_{mk'} + \sigma_z^2}. \quad (10)$$

Then, we know that $\hat{g}_{mk,p} \in \mathbb{C}N(0, \alpha_{mk})$ with $\alpha_{mk} = \frac{p_{mk}^2}{p_u \sum_k c_{pk} \beta_{mk'} + \sigma_z^2}$ and $\bar{g}_{mk,p} \in \mathbb{C}N(0, \beta_{mk})$, in comparison with the actual CSI $g_{mk,p} \in \mathbb{C}N(0, \beta_{mk})$.

B. Downlink Data Transmission

Without loss of generality, we assume that CSI keeps constant during the data transmission. The real downlink channel matrix is denoted by $G \in \mathbb{C}^{K \times M}$, where the entry on the $k^{th}$ row and the $m^{th}$ column is $g_{km,d} = g_{mk,d}$ due to channel reciprocity. But the system only knows $\hat{G}$ consisting of $\hat{g}_{mk,d}$ that is not only an estimate but also an aged version of $G$. With the precoded symbol vector $x = [x_1, \ldots, x_M]^T$, the received symbol vector $y = [y_1, \ldots, y_K]^T$, and the transmit power limit of AP $p_d$, the DL data transmission is expressed by

$$y = \sqrt{p_d} G x + z. \quad (11)$$

Using ZF, we get the precoded symbol vector as $x = \hat{G}^H \left( \hat{G} \hat{G}^H \right)^{-1} P_s$, where $P \in \mathbb{C}^{K \times K}$ is a diagonal matrix consisting of power-control coefficients, i.e., $P = \text{diag}[\eta_1, \ldots, \eta_K]$. Then, (11) can be rewritten as

$$y = \sqrt{\rho_{sd}} \hat{G}^H \left( \hat{G} \hat{G}^H \right)^{-1} P_s + z. \quad (12)$$

IV. PERFORMANCE ANALYSIS

According to (6), the overall CSI during the DL data transmission is obtained:

$$g_{mk,d} = \sqrt{\beta_{mk} h_{mk,d} e^{j (\phi_{kd} + \phi_{kd})}}. \quad (13)$$

The innovation component in (13) corresponds to a compound element in the overall CSI, which we write as $e_{mk} = \sqrt{\beta_{mk} \beta_{mk} e^{j (\phi_{kd} + \phi_{kd})}}$ for ease of derivation. Substituting (13) into (14) and applying (9), we have

$$g_{mk,d} = \rho_{kd} \hat{g}_{mk,p} + e_{mk} \sqrt{1 - \rho_{kd}^2} e^{j (\phi_{kd} + \phi_{kd} - \phi_{kd} - \phi_{kd})} \quad (14)$$

$$= \rho_{kd} \hat{g}_{mk,p} + e_{mk} \sqrt{1 - \rho_{kd}^2} e^{j (\phi_{kd} - \phi_{kd} - \phi_{kd} + \phi_{kd})} \quad (15)$$

We denote the $k^{th}$ row of $\hat{G}$ as $\hat{g}_k = [\hat{g}_{k1,p}, \ldots, \hat{g}_{KM,p}]$, while defining $\hat{G} = [\hat{g}_{1,k}, \ldots, \hat{g}_{MK,k}]$, $\hat{e}_k = [e_{1k}, \ldots, e_{MK}]$, and a diagonal matrix $\Delta \Phi = \text{diag}[e^{j (\phi_{kd} - \phi_{kd})}, \ldots, e^{j (\phi_{kd} - \phi_{kd})}] \in \mathbb{C}^{M \times M}$. Building a channel vector $\hat{g}_{kd} = [\hat{g}_{1kd}, \ldots, \hat{g}_{MKd}] \in \mathbb{C}^{K \times M}$ and substituting (15) into it, yields

$$\hat{g}_{kd} = e^{j (\phi_{kd} - \phi_{kd})} (\rho_{kd} \hat{g}_k + e_{mk} \sqrt{1 - \rho_{kd}^2} e^{j (\phi_{kd} - \phi_{kd})} \Delta \Phi \quad (15)$$

with several steps manipulation. From (12), we can get the received signal of UE $k$, i.e., $y_k = \sqrt{\rho_{sd}} \hat{g}_{kd} \hat{G}^H \left( \hat{G} \hat{G}^H \right)^{-1} P_s + z_k$, like (2). Using (15), the received signal can be decomposed, as given by (16). During the derivation, we apply $T_{PN} =$
\[
\gamma_k = \sqrt{p_d}g_k\hat{E}\left(\hat{G}\hat{G}^H\right)^{-1}P + z_k
\]
\[
= \sqrt{p_d}e^{i(\xi_{k\nu} + \xi_{k\nu})} \rho_k g_k + \sqrt{1 - \rho_k^2}e_{k\nu} + \Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P + z_k
\]
\[
= \sqrt{p_d}e^{i(\xi_{k\nu} + \xi_{k\nu})} \rho_k g_k + \sqrt{1 - \rho_k^2}e_{k\nu} + \Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P + \sqrt{p_d(1 - \rho_k^2)}e^{i(\xi_{k\nu} + \xi_{k\nu})} \rho_k g_k \Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P + z_k
\]

\[\begin{align*}
\mathbb{E}[I_1^2] &= \mathbb{E}\left[\sqrt{p_d}e^{i(\xi_{k\nu} + \xi_{k\nu})} \rho_k g_k \Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P \right]^2 \\
&= p_d\rho_k^2 \mathbb{E}\left[|g_k\Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P|\right]^2
\end{align*}\]

\[\begin{align*}
\mathbb{E}[I_2^2] &= \mathbb{E}\left[\sqrt{p_d(1 - \rho_k^2)}e^{i(\xi_{k\nu} + \xi_{k\nu})} \rho_k g_k \Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P \right]^2 \\
&= p_d\rho_k^2 \mathbb{E}\left[|g_k\Phi\hat{G}\hat{G}^H \left(\hat{G}\hat{G}^H\right)^{-1}P|\right]^2
\end{align*}\]

\[\lim_{M \to \infty} \frac{1}{\sqrt{K}} \text{tr}(\Delta \Phi) = e^{-n_\text{ severity}^2/2} \] according to (16), where the phase noise hardens to a deterministic value when \(M \to \infty\).

The transmit symbols, estimation errors, innovation components, and additive noise are independent, such that the terms \(D, I_1, I_2,\) and \(I_3\) are mutually uncorrelated. By using the fact that uncorrected Gaussian noise represents the worst case (1), the achievable SE is lower bounded by \(\log_2(1 + \gamma_k)\) with the effective signal-to-interference-plus-noise ratio (SINR)

\[
\gamma_k = \frac{\mathbb{E}[D^2]}{\mathbb{E}[I_1^2] + \mathbb{E}[I_2^2] + \mathbb{E}[I_3^2]}.
\]

It is easy to know \(\mathbb{E}[D^2] = p_p \rho_\text{ ISS} e^{-n_\text{ severity}^2} \) and \(\mathbb{E}[I_3^2] = \sigma_i^2\). Similar to Theorem 1 of [2], we can figure out \(\mathbb{E}[I_1^2]\), as given by (17) at the top of this page, where \(D_k = \mathbb{E} \left( g_k \hat{G} \right) = \text{diag}(\beta_1 \alpha_1, \beta_2 \alpha_2, \ldots, \beta_M \alpha_M) \in \mathbb{C}^{M \times M}\) is a diagonal matrix, and \(\hat{G}\) denotes the \(i\)th diagonal element of \(\mathbb{E}\left( \hat{G}\hat{G}^H \right)^{-1} \hat{G} D_k \hat{G}^H \left( \hat{G}\hat{G}^H \right)^{-1}\). Likewise, \(\mathbb{E}[I_2^2]\) is given by (18), where \(E_k = \mathbb{E} (e_k^H e_k) = \text{diag}(\beta_1, \beta_2, \ldots, \beta_M) \in \mathbb{C}^{M \times M}\), and \(\chi_{ki}\) represents the \(i\)th diagonal element of \(\mathbb{E}\left( \hat{G}\hat{G}^H \right)^{-1} \hat{G} e_k \hat{G}^H \left( \hat{G}\hat{G}^H \right)^{-1}\). Substituting (17) and (18) into (19), we get

\[
\gamma_k = \frac{\rho_k^2 \eta_k + (1 - \rho_k^2) \sum_{i=1}^{K} \eta_i \chi_{ki} + \sigma_i^2}{\rho_k e^{-n_\text{ severity}^2}}.
\]

Taking into account the propagation delay over the air interface \(n_{ai} = \left| \sum_{j=1}^{M} \frac{d_j}{c} \right|\) and the delay \(n_{\Delta r}\), the achievable spectral efficiency of the \(k\)th user is

\[
R_k = (1 - \frac{n_{ai} + n_{\Delta r}}{T_b}) \log_2 (1 + \gamma_k).
\]

Fig. 2. The CDF comparison under different values of user mobility and phase noise. The curve of perfect CSI in stationary state \(v = 0\) km/h with perfect oscillators \(T_{YN} = 0^\circ\) is applied as the benchmark.

Fig. 3. The 5%-likely and median per-user SE with respect to correlation coefficient (left) and phase noise (right). The straight lines are 5%-likely and median per-user SE of the benchmark, respectively.

V. NUMERICAL EXAMPLES

This section illustrates some representative numerical results to observe the impact of channel aging on the downlink of
which is equivalent to very high correlation

stationary

eff

effect of phase noise is investigated by using the selected phase noise

high loss of 97% and 86%, respectively. In addition, the impact

mobility of

values:

decrease to 0

62.

formance deterioration is already remarkable. To be specific,

delay. Numerical results revealed that both user mobility and

phase noise affect the performance remarkably, while the aging

effect due to user mobility is more severe. Consequently,

the effect of channel aging should be seriously considered
during the design of zero-forcing precoding and delay-tolerant

schemes such as channel prediction [17] are necessary for the practical deployment of cell-free massive MIMO.

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