Kinematical trends among the field horizontal branch stars

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Abstract. Horizontal branch (HB) stars in the field of the Milky Way can be used as tracers for the study of early stages of the evolution of our galaxy. Since the age of individual HB stars is not known a priori, we have studied the kinematics of a sample of field HB stars measured with Hipparcos to look for signs of age and population nature. Our sample comprises 14 HBA, 2 HBB and 5 sdB/O stars. We found that the kinematics of the HBA stars is very different from that of the sdB/O stars (including those from an earlier study). The HBA stars have low orbital velocities, some are even on retrograde orbits. Their orbits have large eccentricities and in many cases reach large distances above the galactic plane. In contrast, the sdB/O stars show disk-like orbital characteristics. The few HBB stars (with $T_{\text{eff}} > 10,000$ K) in our sample seem to have kinematics similar to that of the sdB/O stars.

In order to see if there is a trend among the HB stars in their kinematics, we investigated also RR Lyrae stars measured with Hipparcos. Here we found a mixed kinematical behaviour, which was already known from previous studies. Some RR Lyrae stars have disk-like orbits (most of these being metal rich) but the majority has halo-like orbits, very similar to those of our HBA stars.

Since the atmospheres of most types of HB stars do not reflect original metallicities any more the kinematics is the only aspect left to study the origin and population membership of these stars. Thus, the clear trend found in kinematics of stars along the HB, which is also a sequence in stellar mass, shows that the different kinds of field HB stars arose from stars having different origins in age and, e.g., metallicity or mass loss rate.

Key words: Stars: kinematics – Stars: horizontal branch – Stars: Population II – Galaxy: halo – Galaxy: kinematics and dynamics – Galaxy: structure

1. Introduction: HB-stars, their population membership and the galactic structure

Stars of horizontal-branch nature are important objects in studies of the older stellar populations and in studies of galactic structure in relation with formation theories for the Milky Way. Their virtue lies in three properties. First, they have rather well defined absolute magnitudes and their distances are therefore easy to determine. Second, their nature is such that they are easy to discover, in particular at higher galactic latitudes. Third, the stellar evolution leading to such stars is in principle relatively well understood.

The horizontal branch (HB) stellar phase is the core helium burning late stage of evolution of originally low to medium mass stars. During the red giant phase the stars have lost mass such that a helium core of $\approx 0.5 M_\odot$, surrounded by an outer shell of hydrogen gas, remains. For very thin shells, $M_{\text{shell}} < 0.02 M_\odot$, the stars are rather blue and of spectral class sdB (subdwarf B), for ever thicker shells their atmospheres are cooler, leading to spectral types such as horizontal branch B and A (HBB and HBA) and to the red HB (RHB) stars with $M_{\text{shell}} \approx 0.5 M_\odot$. Between the HBA and RHB stars lies the pulsational instability strip with the RR Lyrae stars. (For the systematics of the spectral classification see de Boer et al. 1997c.) HBA and HBB stars are often called blue HB (BHB) stars, the even hotter sdB and sdO stars are also known as extended or extreme HB (EHB) stars.

BHB and EHB stars can be easily found based on their blueness, the RR Lyr stars due to their variability. Of the BHB stars, the HBAs are easily identified, as their physical parameters differ from main sequence A stars, while HBBs may be confused with main sequence B stars. However, at higher galacttical latitudes A or B main sequence stars are very rare. RHB stars can easily be confused with subgiants and giants because they lie in the same region of the HRD.

To trace the structure of the (local part of the) Milky Way one employs several techniques (see also the review by Majewski 1993). The classical method is to perform star counts (see, e.g., Bahcall & Soneira 1984). Selecting stars based on their proper motion allows, if their radial
velocities and distances are also determined, to study the true kinematics of the stars (see, e.g., Carney et al. 1996 and papers cited there). Basing oneself on proper motions one naturally studies the general group of more nearby stars extended by true high-velocity stars. Another method is to sample distances and radial velocities of a specific set of stars, such as BHB or RR Lyr stars, to investigate these parameters in a statistical manner (see, e.g., Kinman et al. 1994, 1996). A more specific method is to observe statistically complete samples of stars of a special type in several directions to derive scale heights (for sdB stars see e.g., Heber 1986, Moehler et al. 1990, Theissen et al. 1993), or scale lengths in the Milky Way. A further possibility is to go beyond the present kinematic parameters by calculating orbits based on distances, radial velocities, and proper motions. This method has been used for high proper motion stars (Carney et al. 1996), other dwarf stars (Schuster & Allen 1997), and for globular clusters (Dauphole et al. 1996). Also the orbits of sdB stars have been investigated (Colin et al. 1994, de Boer et al. 1997a). The latter study showed that most of the sdB stars have orbits staying fairly well inside the Milky Way disk, indicating that the sdB stars are not generally part of the halo population.

In the present study we have attempted to perform a similar analysis for HBA and HBB stars (for short: HBA/B stars). Our sample consists of the local HB stars which were observed by the Hipparcos satellite. These are the HB-like stars with the most accurate spatial and kinematic data available to date.

However, only for a few HBA/B stars are the parallaxes accurate enough to calculate reliable distances (de Boer et al. 1997b). For the other stars the distance still must be derived from photometry. Here one needs to know the absolute magnitude of field horizontal branch stars. Especially since the publication of the Hipparcos catalogue a lot of effort has gone into fixing this value. However, this has not yet led to total agreement. For a review of various approaches to solving this problem we refer to de Boer (1999) and Popowski & Gould (1999).

An important parameter in these studies is the metallicity of the stars, as it is generally thought to be correlated with age. For dwarf stars metallicities can be estimated using photometric indices or spectroscopy (see the summary by Majewski 1993). For HB stars this is, unfortunately, not a trustworthy method. The atmospheres of many HB stars have most probably been altered chemically with respect to the original composition. Gravitational settling of heavy elements in the sdB/O star and possibly HBB star atmospheres leads to a present lower content of elements like He, while levitation of heavy elements leads to atmospheres with enhanced abundances of certain elements like Fe or Au as found in several field horizontal branch stars, e.g. Feige 86 (Bonifacio et al. 1995). Levitation must also be the explanation for the high metal abundances in blue HB stars in M 13 (Behr et al. 1999) and NGC 6752 (Moehler et al. 1999) finally uncovered to explain deviant flux distributions near the Balmer jump of globular cluster blue HB stars (Grundahl et al. 1999). Therefore, original metallicities (as well as the original masses) are no longer accessible quantities. Determining the kinematic properties can help deciding which of the HB stars are intrinsically more metal poor and which are more metal rich, and hence of somewhat younger origin.

The main subjects of our study are the HBA/B stars which are located in the colour magnitude diagram on the horizontal branch between the RR-Lyrae stars and the hot subdwarfs. Unfortunately the main sequence crosses the HB at the HBB region, so that HBB stars can be confused with normal B stars. Therefore we have only few HBB stars in our sample. We mainly focus on HB stars with temperatures lower than 10000 K which lie above the main sequence.

Sect. 2 deals with the data necessary for our study. In Sect. 2.3 we determine the absolute magnitudes and distances of the HBA/B and sdB/O stars with the method of auto-calibration using the shape of the HB defined by the stars with the best Hipparcos parallaxes. In Sect. 3 we discuss the kinematical behaviour of the HBA/B and sdB/O stars and make comparisons with the results of de Boer et al. (1997a). To further explore a possible trend in kinematics of stars along the HB we investigate (Sect. 4) the orbits of a sample of RR-Lyrae stars.

2. The data

2.1. Composition of the sample

Our sample consists of the Hipparcos (ESA 1997) measured HB stars. In order to identify them we searched through lists of bright HB-candidates in publications concerning horizontal branch stars, such as Kilkenny et al. (1987) for sdB/O stars, and Corbally & Gray (1996), Huenemoerder et al. (1984), and de Boer et al. (1997b) for the HBA/B stars. However, for a few stars in these lists indications exist that they are probably not horizontal branch stars. Among these are HD 64488 (Gray et al. 1996), HD 4772 (Abt & Morell 1995, Philip et al. 1990), HD 24000 (Rydgren 1971), HD 52057 (Waalkens et al. 1998, Stetson 1991) and HD 85504 (Martinet 1970). This sample, although being of limited size, represents the HB stars with by far the best kinematical data currently available.

Two further stars are HB-like but were excluded from the study nevertheless. BD +32 2188 has a rather low value for log g so that it lies considerably above the ZAHB in the log g – T_{eff} diagram. Being metal deficient (Corbally & Gray 1996) it can be considered a horizontal branch star evolving away from the ZAHB. Because the evolutionary state is not fully HB the star cannot be part of our sample. HD 49798 is a subluminous O-star. However, its log g is relatively low and its trigonometrical parallax implies a
star with absolute brightness of about $-2$ mag, far too bright for a normal sdO star. It is probably on its way from the horizontal branch to become a white dwarf or it is a former pAGB star. Because of these aspects we excluded this star.

A large fraction of the known horizontal branch stars has no published radial velocity and could therefore not be used for our study. A few stars had radial velocities but no Hipparcos data.

There is no constraint on the position, so that the sample stars are located in all parts of the sky. However, as many studies were made in fields near the galactic poles we have relatively more stars at very high galactic latitudes. Although our sample of stars is certainly not statistically complete in any way, we do not expect noticeable selection effects due to position in the sky (see Sect. 5.2.).

### 2.2. Physical properties of the stars, extinction

2.2. Physical properties of the sample of horizontal branch stars.

### Table 1. Physical properties of the sample of horizontal branch stars.

| Name          | HIP    | $V^a$ | $B - V^a$ | $E_{B-V}^b$ | $\delta M_V^b$ | Type$^c$ | $T_{eff}$ | log $g$ | Source$^d$ |
|---------------|--------|-------|-----------|-------------|---------------|----------|----------|--------|-----------|
| HD 2857      | 2515   | 9.967 | 0.219     | 0.050       | -0.001        | HBA      | 7700     | 3.1    | GCP, HBC  |
| HD 14829     | 11124  | 10.228| 0.023     | 0.020       | -0.580        | HBA      | 8700     | 3.3    | GCP      |
| HD 60778     | 36899  | 9.131 | 0.135     | 0.020       | -0.640        | HBA      | 8600     | 3.3    | GCP, S91, HBC |
| HD 74721     | 43018  | 8.717 | 0.042     | 0.000       | -0.330        | HBA      | 8600     | 3.3    | GCP, S91, HBC |
| HD 78913     | 44734  | 9.291 | 0.094     | 0.300       | -0.215        | HBA      | 8700     | 2.5    | IUE-fit, S91 |
| HD 86986     | 49198  | 8.000 | 0.119     | 0.035       | -0.130        | HBA      | 7900     | 3.1    | B97b, S91 |
| BD +36 2242  | 59252  | 9.904 | -0.065    | 0.010       | -1.188        | HBB      | 11400    | 4.4    | HBC      |
| HD 106304    | 59644  | 9.077 | 0.027     | 0.040       | -0.696        | HBA      | 9500     | 3.0    | IUE-fit, S91 |
| BD +42 2309  | 60854  | 10.820| 0.043     | 0.000       | -0.324        | HBA      | 8400     | 3.3    | GCP      |
| HD 109995    | 61696  | 7.603 | 0.047     | 0.001       | -0.307        | HBA      | 8300     | 3.15   | B97b, S91 |
| BD +25 2602  | 64196  | 10.148| 0.057     | 0.065       | -0.659        | HBA      | 9200     | 3.4    | GCP, S91, HBC |
| HD 117880    | 66411  | 9.059 | 0.082     | 0.015       | -0.201        | HBA      | 7500     | 2.95   | B97b, S91 |
| Feige 86     | 66541  | 10.006| -0.140    | 0.050       | -2.193        | HBB      | 15300    | 4.1    | HBC      |
| HD 130095    | 72278  | 8.155 | 0.032     | 0.064       | -0.840        | HBA      | 8800     | 3.15   | B97b, S91 |
| HD 139961    | 76961  | 8.857 | 0.098     | 0.107       | -0.666        | HBA      | 8750     | 3.3    | B97b, S91 |
| HD 161817    | 87001  | 7.002 | 0.166     | 0.020       | -0.001        | HBA      | 7500     | 2.95   | B97b, S91 |
| CD −38 222   | 3381   | 10.400| -0.224    | 0.013       | -2.639        | sdB      | 28200    | 5.5    | B97b, B97a |
| Feige 66     | 61602  | 10.602| -0.286    | 0.040       | -3.556        | sdB      | 28000    | 4.9    | KHD, S94 |
| HD 127493    | 71096  | 10.040| -0.251    | 0.095       | -3.756        | sdO      | 40000    | 5.8    | KHD      |
| HD 149382    | 81145  | 8.872 | -0.280    | 0.050       | -3.598        | sdOB     | 40000    | 5.8    | KHD, S94 |
| HD 205805    | 106917 | 10.158| -0.241    | 0.025       | -2.929        | sdB      | 25000    | 5.0    | B97b, B97a |

(1) $V$, $B - V$ from the Hipparcos Catalogue

(2) $E_{B-V}$, $\delta M_V$, see Sect. 2.2 and 2.3

(3) Type: HBA stars: $T_{eff} < 10500$ K; HBB stars: $20000$ K $> T_{eff} > 10500$ K; sdB/O stars: from literature (see under source)

(4) The values for $log g$ and $T_{eff}$ have been taken from the first work cited. HBC: Huenemoerder et al. (1984); GCP: Gray et al. (1996), B97a: de Boer et al. (1997a), B97b: de Boer et al. (1997b), KHD: Kilkenny et al. (1987) and references therein, S91: Stetson (1991), S94: Saffer et al. (1994), IUE-fit: see Sect. 2.2

2.3. Absolute magnitudes and distances

We obtained the distances of the HB stars using the absolute magnitude of the relevant portion of the HB rather than directly using the Hipparcos parallaxes. The reason for this is that most of the parallaxes are smaller than 3 mas which means that their error of on average 1 mas is too large to calculate accurate distances. The absolute magnitudes $M_V$, which are a function of the temperature...
We started with the determination of the shape of the field horizontal branch. For this we calculated the absolute magnitudes of those HB and sdB/O stars which have reasonably good parallaxes. For the determination of the mean absolute magnitude of the HB sample we excluded HD 74721 and BD +42 2309 because their absolute magnitudes, calculated from their parallaxes, are too bright by more than 3.5 magnitudes. Also excluded at this point are HD 139961, whose parallaxes lead to absolute magnitudes far too faint. With this medianization (leaving out the extremes to both sides) we ensure that our result is not affected by stars with extreme values. Furthermore the stars having parallaxes with $\Delta \pi / \pi > 1$ were excluded for the determination of the shape of the HB.

We then fitted by eye a curve to our sample in the colour magnitude diagram. In order to smooth this curve, it was approximated by a polynomial. Note that we aim to fit the observed parameters of the field horizontal branch and that we do not rely on a shape taken from globular clusters or theoretical models (see Fig. 1).

From this we determined the value $\delta M_V$ giving the difference of $M_V$ for each $(B - V)_0$ with respect to $M_V$ at $(B - V)_0 = 0.2$ mag. Although the available metallicity measurements show a large spread for individual stars (see Table II of Philip 1987), the averages for each lie around $[\text{Fe/H}] \sim -1.5$ dex. Since the effect of metallicity on $M_V$ is small for RR Lyr stars (about 0.1 mag per 0.5 dex, see de Boer 1999) we will neglect the metallicity effects for the HBA stars.

Distances and absolute magnitudes of a sample of stars obtained through trigonometric parallaxes have to be corrected for the Lutz-Kelker bias (Lutz & Kelker 1973). This statistical effect, depending on the relative error of the parallaxes, leads to an over-estimation of the parallax on average, leading to too faint absolute magnitudes and too short distances of the sample.

The correction we applied is based on the averaging of parallaxes. For that we have to correct the parallaxes of individual stars, acknowledging that such a correction is only valid in a statistical sense. The expected parallax $\pi^*$ given by

$$\pi^* = 10^{0.2[M_V - V - \delta M_V] - 1 + 0.62E_{B-V}}$$

(1)

with $M_V$ being the absolute magnitude, $V$ the apparent magnitude, $E_{B-V}$ the reddening, $\delta M_V$ is a term which accounts for the temperature and/or $B - V$ dependence of the absolute magnitude of BHB stars in the same way.
Fig. 1. Colour magnitude diagram showing the stars of our sample and the curve which was used as the shape of the FHB.

Hexagons: HBA/B stars (open symbols mean stars not used for the fit), crosses mean sdB/O stars, the square depicts RR Lyrae.

as done by Gratton (1998). Now $M_V$ is varied and 

$$\chi^2(M_V) = \sum_i (\pi_i(M_V) - \pi_i)^2/(\Delta \pi_i)^2$$

is calculated (formula as revised by Popowski & Gould 1999). At the correct $M_V$ the average of $\chi^2$ should be minimized.

$M_V$ is now found using all stars, regardless of their $\Delta \pi/\pi$, except the four excluded above. We arrived at an absolute magnitude of $M_V = 0.63 \pm 0.08$ mag for the horizontal part ($B-V)_0 \sim 0.2$ mag) of the horizontal branch. As stated before this value should be valid for [Fe/H] $\sim -1.5$ dex. However, as the curve defining the shape of the HB is subjective to a certain extent the real error of the HB’s absolute magnitude is somewhat larger. The absolute magnitudes and thus the distances of the individual stars including those omitted earlier are obtained by adding their $\delta M_V$ to the mean absolute magnitude of the HB.

2.4. Proper motions and positions

Positions and proper motions used in this work were taken from the Hipparcos catalogue (ESA 1997). The mean error of the proper motions is below 1.5 mas/yr (see Table 2) which means an error in the tangential velocity of 3.5 km s$^{-1}$ for a star at a distance of 500 pc. As most of our stars have smaller distances the error caused by the proper motion uncertainty is even smaller.

No star of the sample of HBA/B or sdB/O stars has an astrometric flag in the Hipparcos catalogue, indicating there were no problems in the data reduction. The Hipparcos goodness-of-fit statistic is below +3 in all cases, meaning that the astrometric data derived from the Hipparcos catalogue should be reliable and there are no indications that our sample contains double stars.

2.5. Radial velocities

The radial velocities were taken from original sources (see Table 2), in part found from the Hipparcos Input Catalogue (Turon et al. 1987). The typical uncertainties are about 10 km s$^{-1}$, so that they should not have a large effect on our results. The size of our sample was limited to a large extent by the lack of radial velocities; for only about 30% of the HB-candidates radial velocities could be found.

Radial velocities can be affected by binarity of the star. We cannot absolutely exclude this possibility for some of the stars, but as noted in Sect. 2.4 there are no indications for binary nature for any of our stars.

For some stars, Corbally & Gray (1996) found drastically different values for the radial velocity. They note however that in many of these cases their values may be affected for some reason (see their Sect. 4) as they show strong deviations with respect to values from the literature. We therefore used radial velocities from Corbally & Gray only for HD 2857 for which no other value is available.

3. Kinematics and orbits

In order to gain information about the nature and population membership of the stars we analyse their kinematic behaviour and calculate their orbits.

3.1. Calculating orbits and velocities

Before calculating the orbits the observational data have to be transformed into the coordinates of the galactic system $(X, Y, Z; U, V, W)$. In this coordinate system $X$ points from the Sun in direction of the galactic centre with its origin in the galactic centre, $Y$ points into the direction of the galactic rotation at the position of the sun, and $Z$ toward the north galactic pole. The same applies to the corresponding velocities $U, V, W$.

The orbits are calculated using the model for the gravitational potential of our Milky Way by Allen & Santillan (1991) which was developed to be used in an orbit calculating program (Odenkirchen & Brosche 1992). This model has been extensively used in the studies of de Boer et al. (1997a), Geffert (1998) and Scholz et al. (1996). There are several other models available which yield similar results as long as the orbits do not extend to extreme distances from the galactic centre (Dauphole et al.
Note: Due to a change in the convention (see Geffert 1998), the values of \( I_\ell \) have changed their sign (positive \( \Theta \) have now positive \( I_\ell \)) in contrast to previous work (e.g. de Boer et al. 1997a)

### Table 3. Orbital and kinematical characteristics

| Name      | \( R_a \) | \( R_p \) | \( z_{\text{max}} \) | \( ecc \) | \( nze \) | \( U \)  | \( V \)  | \( W \)  | \( \Theta \) | \( I_\ell \) | Type |
|-----------|-----------|-----------|----------------------|----------|--------|--------|--------|--------|-----------|--------|------|
| HD 2857   | 11.81     | 0.44      | 6.47                 | 0.93     | 1.04   | +156   | +25    | +67    | +29       | +251   | HBA  |
| HD 14829  | 11.29     | 2.69      | 8.11                 | 0.62     | 1.01   | +108   | +71    | +156   | +71       | +622   | HBA  |
| HD 60778  | 9.35      | 2.41      | 4.56                 | 0.59     | 0.56   | +53    | +82    | -115   | +80       | +714   | HBA  |
| HD 74721  | 8.65      | 1.95      | 4.42                 | 0.63     | 0.59   | +22    | +70    | -109   | +69       | +606   | HBA  |
| HD 78913  | 9.52      | 1.79      | 0.38                 | 0.68     | 0.05   | +107   | -77    | +24    | -83       | -695   | HBA  |
| HD 86986  | 16.96     | 0.33      | 13.26                | 0.96     | 1.63   | +248   | +24    | +50    | +20       | +217   | HBA  |
| BD +36 2242 | 9.96     | 8.58      | 0.42                 | 0.04     | 0.05   | +3     | +227   | +3     | +227      | +1945  | HBB  |
| HD 106304 | 8.42      | 1.65      | 7.27                 | 0.67     | 1.62   | -22    | +38    | -150   | +39       | +327   | HBA  |
| BD +42 2309 | 9.96     | 0.91      | 5.26                 | 0.83     | 0.89   | +29    | +34    | -110   | +35       | +300   | HBA  |
| HD 109995 | 9.41      | 0.48      | 5.52                 | 0.90     | 1.00   | +4     | +30    | -96    | +30       | +258   | HBA  |
| BD +25 2902 | 10.80    | 1.51      | 1.71                 | 0.75     | 0.18   | -146   | +72    | -53    | +72       | +607   | HBA  |
| HD 117880 | 8.91      | 4.17      | 9.29                 | 0.36     | 4.89   | -55    | -28    | -199   | -26       | -217   | HBA  |
| Feige 86  | 9.18      | 2.95      | 0.27                 | 0.51     | 0.03   | +76    | +117   | -7     | +118      | +995   | HBB  |
| HD 130095 | 8.94      | 0.49      | 5.13                 | 0.90     | 0.93   | -58    | +30    | +65    | +31       | +258   | HBA  |
| HD 139961 | 8.26      | 1.57      | 1.68                 | 0.68     | 0.22   | +3     | -69    | +81    | -69       | -568   | HBA  |
| HD 161817 | 12.51     | 1.30      | 7.36                 | 0.81     | 0.74   | -109   | -54    | -129   | -56       | -473   | HBA  |
| CD -38 222 | 9.31     | 7.29      | 1.23                 | 0.12     | 0.13   | -38    | +206   | +59    | +207      | +1749  | sdB  |
| Feige 66  | 9.10      | 7.76      | 0.22                 | 0.08     | 0.02   | +24    | +217   | +8     | +217      | +1841  | sdB  |
| HD 127493 | 8.53      | 7.71      | 0.20                 | 0.05     | 0.02   | +10    | +212   | +15    | +212      | +1780  | sdO  |
| HD 149382 | 9.64      | 8.33      | 0.13                 | 0.07     | 0.01   | +13    | +233   | +10    | +233      | +1966  | sdB  |
| HD 205805 | 11.48     | 6.72      | 0.19                 | 0.26     | 0.02   | -82    | +225   | -3     | +225      | +1880  | sdB  |

Note: Due to a change in the convention (see Geffert 1998), the values of \( I_\ell \) have changed their sign (positive \( \Theta \) have now positive \( I_\ell \)) in contrast to previous work (e.g. de Boer et al. 1997a)
Fig. 2. Orbits of the HBA/HBB stars displayed in meridional cuts. The orbits shown here have been calculated for 10 Gyr, in order to make the shape of the orbit better visible (The orbit of HD 74721 (similar to HD 60778) is not shown). For orbits of sdB stars see de Boer et al. (1997a).

Table 4. Mean orbital parameters $\Theta$, $ecc$ and $nze$ for various subsamples of HB stars

| Types subsample          | number of stars | $nze$    | $\sigma_{nze}$ | $\Theta$ | $\sigma_{\Theta}$ | $ecc$ | $\sigma_{ecc}$ |
|--------------------------|-----------------|---------|---------------|---------|-------------------|-------|---------------|
| HBA this paper           | 14              | 1.10    | 1.15          | +17     | 52                | 0.74  | 0.16          |
| HBB this paper & Schmidt (1996) | 6              | 0.24    | 0.15          | +151    | 55                | 0.41  | 0.27          |
| sdB/O this paper         | 5               | 0.04    | 0.05          | +218    | 10                | 0.12  | 0.08          |
| sdB this paper & de Boer (1997b) | 44             | 0.25    | 0.17          | +198    | 50                | 0.15  | 0.11          |
| RR Lyr all               | 32              | 0.86    | 1.50          | +80     | 114               | 0.59  | 0.33          |
| RR Lyr $[\text{Fe/H}] > -0.9$ | 7              | 0.08    | 0.05          | +218    | 37                | 0.19  | 0.13          |
| RR Lyr $-0.9 > [\text{Fe/H}] > -1.3$ | 7              | 0.88    | 0.57          | +43     | 109               | 0.64  | 0.38          |
| RR Lyr $-1.3 > [\text{Fe/H}] > -1.6$ | 10             | 1.54    | 2.43          | +32     | 74                | 0.68  | 0.40          |
| RR Lyr $-1.6 < [\text{Fe/H}]$ | 8               | 0.68    | 0.47          | +51     | 107               | 0.65  | 0.30          |

3.2. Morphology of the orbits

The orbits of the HBA/B stars show a large variety of shapes. Nearly all of the cooler HBA stars have a small perigalactic distance ($R_p \leq 3$ kpc) and the most extreme case, HD 86986, reaches a perigalactic distance of only 0.4 kpc. The single exception is HD 117880, which has a $R_p$ of nearly 4 kpc.

Four stars have truly chaotic orbits, the rest has boxy type orbits, but some of these show signs of chaotic be-
haviour as well. HD 79813 has an orbit staying very close to the disc, while HD 117880 orbits nearly perpendicular to the galactic plane. On the whole about half of our stars have orbits which are chaotic or show signs of that. This agrees quite well with the results of Schuster & Allen (1997) who analysed a sample of local halo subdwarfs.

Most of the stars have apogalactic distances of $\approx 8$ to $11$ kpc, just one star (HD 86986) goes well beyond. The reason for this clumping in $R_\alpha$ is not physical but due to selection effects. Stars with $R_\alpha \leq 7.5$ kpc never venture into the observable zone (at least observable by Hipparcos). On the other hand the probability of finding the stars is greatest when they are near their major turning point, $R_p$. So it is clear that the mean $R_\alpha$, as well as to a lesser extent the eccentricity, are affected by selection effects.

Stars belonging to the thin disk would have orbits with very small eccentricities and $n\pi e$ values (solar values: $ecc = 0.09$, $n\pi e = 0.001$, see de Boer et al. 1997a), while thick disk stars would have larger values on average. Halo stars have generally orbits with large eccentricities while their $n\pi e$ show a large range.

The eccentricities of the HBA star orbits are very large, ranging from 0.5 to nearly 1.0, the values for $n\pi e$ vary by a huge amount, from 0.04 (HD 78913) to 5 (HD 117880). The stars BD +36 2242 and Feige 86 are exceptions, their values for both parameters are more appropriate for disk objects. We note that these two stars are the hottest of the HBA/B sample. The kinematics of the four HBB stars from Schmidt (1996) show overall behaviour similar to that of BD +36 2242 and Feige 86 (Fig. 2). All of these are hotter than 11000 K, the $T_{\text{eff}}$ of BD +36 2242.

The star HD 117880 features an orbit somewhat dissimilar from the others. While its $n\pi e$ is very high, its eccentricity is by far the lowest of the sample of HBA stars.

3.3. Velocity components and dispersions

The HBA stars ($T_{\text{eff}} \leq 10,000$ K) have a mean orbital velocity of $\Theta = 17$ km s$^{-1}$, lagging about 200 km s$^{-1}$ behind the local standard of rest. However, the velocity dispersions are large: 102, 53 and 95 km s$^{-1}$ in $U$, $V$, $W$ respectively. This shows that there are many stars with a non disk-like kinematical behaviour in the sample of HBA/B stars. They therefore belong to the galactic halo population rather than to the disk.

The orbital velocities of the HBA stars in the sample do not have a Gaussian distribution, as one might have expected. Instead, they seem to have a somewhat flatter distribution (see Fig. 4). About 75% of our stars have prograde velocities, four stars have retrograde orbits. However the exact distribution cannot be studied reliably due to the limited number of stars at disposal.

Both the analysis of the kinematic properties and the shapes of the orbits imply that the HBA/B stars mostly are members of the galactic halo population. However, there seems to be a difference in kinematics and hence population membership between the cooler and the hotter stars. Stars cooler than about 10,000 K have low orbital velocities and a large spread in $n\pi e$. In contrast to this are the hotter stars whose kinematics and orbits are consistent with those of disk objects. The HBB stars of Schmidt (1996) which are all hotter than 10,000 K behave like sdB stars, too.

3.4. Kinematics of sdB/O stars

The sample of sdB/O stars show classical disk behaviour: Their mean orbital velocity is $\Theta = 219$ km s$^{-1}$, meaning a negligible asymmetric drift. The $V$ velocity dispersion (which is also the dispersion in $\Theta$, because the stars are in the solar vicinity) is relatively small, similar to that of thin disk orbits, while the dispersion in $U$ is much larger, fitting to thick disk values. The dispersion $\sigma_W$ is somewhere in between. These values are quite similar to those of the sdB star sample of de Boer et al. (1997a). Until now no population of field sdB stars with halo kinematics has been found. Yet, hot subdwarfs of the horizontal branches of halo globular clusters are, of course, well known (see e.g. Moehler et al. 1997).

3.5. Trend of kinematics along the HB?

Given the results above there seems to be a trend in the kinematics of star types along the blue part of the horizontal branch (see Fig. 3). The sdB/O stars have disklike orbits. The same probably applies to the HBB stars hotter than about 10,000 K, though the statistics are rather poor for this part of the HB. In contrast to that stand the cooler HBA stars which have much smaller orbital velocities, large orbital eccentricities and large ranges of $n\pi e$, thus showing a behaviour fitting more to halo than to disk objects.

This result suggests to analyse the kinematics of the adjoining cooler stars of the HB, the RR Lyraes.

4. RR Lyrae stars

4.1. A sample of RR Lyrae stars from the literature

Recently, Martin & Morrison (1998) carried out an investigation of the kinematics of RR Lyrae stars which is mainly based on the study of Layden (1994). For our analysis we will use only those stars having Hipparcos data. Six Hipparcos stars were excluded because they have a proper motion error larger than 5 mas/yr.

The RR Lyrae stars present the observational difficulty in that they are variables with both $V$ and $B - V$ changing continuously. For most of the sample we were able to take the mean magnitudes from Layden (1994). For the remaining stars we derived the intensity-mean magnitudes with help of the formula given by Fitch et al. (1966) and
Fig. 3. a-b. Kinematical trend of stars along the field horizontal branch characterized by the orbital velocity ($\Theta$) as plotted against effective temperature $T_{\text{eff}}$ and $B - V$.

Panel a: $\Theta$ versus $T_{\text{eff}}$. Filled symbols show the stars with Hipparcos data (Table 3), open symbols are sdB stars of de Boer et al. (1997a) and HBB stars of Schmidt (1996). The symbol shapes represent: hexagons HBA/B stars; squares sdB/O stars.

Panel b: $\Theta$ versus $B - V$, highlighting the cooler part of the HB and including RR Lyrae stars (see Sect. 4). The RR-Lyrae stars are plotted with pentagons subdivided according to $[\text{Fe/H}] < -1.6$ dex (full), $-1.6$ dex $\leq [\text{Fe/H}] < -1.3$ dex, $-1.3$ dex $\leq [\text{Fe/H}] < -0.9$ dex and $[\text{Fe/H}] \geq -0.9$ dex (open symbols).

revised by Barnes & Hawley (1986) which is the same method as used by Layden (1994), using the photometric data of Bookmeyer et al. (1977). The Layden photometry was dereddened using the Burstein & Heiles (1982) reddening maps.

For later steps in this study it is necessary to know the mean $B - V$ of the RR Lyrae stars. As the colour curves of the stars are quite similar to the brightness curves, with the star being bluest when it is near maximum brightness, we took the same formula as we used to calculate the mean magnitude. This is not entirely correct but gives $B - V$ close to the actual one. For six stars we did not have the appropriate light curve data, so we could not determine the mean $B - V$ for them. Therefore only 26 RR Lyraes are shown in Fig. 3.

As the RR-Lyrae stars are in most cases fainter and therefore farther away than our HBA/B stars they have a rather large $\Delta_\pi/\pi$. For this reason we used the absolute magnitude derived in Sect. 2.3 to calculate the distances for these stars. We thus have ignored the effects of metallicity on $M_V$ for individual stars. Also possible evolutionary effects on $M_V$ (see Clement & Shelton 1999) have been ignored, an aspect Groenewegen & Salaris (1999) did not consider in their determination of the RR Lyrae $M_V$ either. Since we study the orbits of the RR Lyrae as a sample these limitations will not affect our conclusions.

For most RR Lyrae stars we took the radial velocities from the sources mentioned in Sect. 2.5, supplemented by radial velocities from Layden (1994).

The metallicities of the RR-Lyrae stars were taken from Layden (1994) as far as possible. A few values come from Layden et al. (1996) and Preston (1959).

4.2. RR-Lyrae kinematics

We calculated the orbits for the RR Lyrae stars in the same manner as for the HBA/B and sdB stars. The RR-Lyrae stars show a spread in kinematical behaviour wider than that of the HBA/B stars. Many stars have orbits similar to those of the HBA stars, others show disklike orbits with orbital velocities in the vicinity of 200 km s$^{-1}$. Of the halo RR-Lyrae stars many have perigalactic distances smaller than 1 kpc, as we also found for the HBA stars. The RR-Lyrae stars have orbital velocities typically spanning the entire range found for disk and halo stars (see Fig. 3). Three members of our sample of RR Lyr stars have orbits shaped somewhat different from those of the rest of halo orbits, looking similar to that of HD 117880.
In Fig. 3 we have sorted the RR Lyr stars according to their metallicity using different plot symbols. The stars with an [Fe/H] $> -0.9$ dex have high Θ like disk stars. The stars with lower metallicities are more evenly distributed in Θ. There are several stars with disk-like kinematics with a very low metallicity as low as [Fe/H] $< -2.0$ dex (see Table 4).

5. Selection effects

The study of the spatial distribution of HB stars involves, unfortunately, several selection effects. The general aspects have been reviewed by Majewski (1993) and will not be repeated in detail here. Yet, for each stellar type discussed in this paper a few comments are in place.

HBA stars have in most cases been identified from photometry, notably because of a larger than normal Balmer jump. This larger jump is mostly due to lower metallicity of the stellar atmosphere. If the atmospheric metallicity is identical to the original one, then the criterion favours intrinsically metal poor stars, which are presumably the older ones. However, also stars starting with a little more mass than the Sun and thus of solar composition will become HB stars and, when as old as the Sun, by now are solar metallicity HB stars. If they were of HBA type, they would not have been recognized in photometry of the Balmer jump. Such stars would be underrepresented in our sample. The HBA stars considered here come from all galactic latitudes, so that selection effects due to galactic latitude are not to be expected. However stars which have orbits going far away from the disk are always underrepresented, as their fraction of time near the disk (and hence being observable) is much smaller than for those which do not go far from the disk.

RR Lyraes, being variables, are not prone to such selection effects. Most of them are identified solely by their variability. Metallicity or high velocity are generally not used as criteria for the identification for RR Lyrae stars. For a discussion of selection effects due to galactic latitude we refer to Martin & Morrison (1998), as our sample is a subsample of theirs.

The sdB/O stars were identified in surveys for quasars, e.g. the PG catalogue (Green et al. 1986) or Hamburger Quasar Survey (Hagen et al. 1995). This means their blue colour is the criterion, rather than proper motion, radial velocity or metallicity. Therefore we do not expect a selection bias towards metal poor halo stars. Moreover, de Boer et al. (1997a) showed that the sdB/O stars observed now near the Sun come from widely differing locations in the Milky Way. As these catalogues only map objects which are somewhat away from the galactic plane, they miss the majority of stars with solar type orbits. sdO stars may be confused with pAGB stars descending down the HRD towards the white dwarf regime.

The HBB stars of Schmidt (1996) are also taken from the PG catalogue, so that there should not be noticeable selection effects, either. However HBB stars and main sequence stars have similar physical properties such as log $g$, so that there may be confusion with the latter. Apart from this the selection effects mentioned for the sdB/O stars apply to the HBB stars, too.

Finally, some words concerning the distribution of distances of the different samples are in place. Generally, if one deals with stars having different absolute magnitudes, as in our case when the sdBs are several magnitudes fainter than the HBAs, one gets samples with different mean distances. The intrinsically fainter stars are on average much nearer than the brighter stars, if the two groups have similar apparent magnitudes. This means that the spatial re-
regions sampled differ depending on the absolute magnitude of the stars. This would imply that the sdB sample is biased towards disk stars as we do not sample them far enough from the galactic plane where there may be a higher concentration of halo stars than further in. This is however not the case. As we include some of the results of de Boer et al. (1997a) which come from a completely different source, namely mostly from the PG-catalogue (Green et al. 1986) dealing with significantly fainter stars, the PG stars actually have on average larger distances than any of our HBA stars. For this reason we do not expect that the difference in kinematics arises from the distribution of the distances in the samples.

6. Discussion: trends and population membership

6.1. Overall trends

As shown in Figs. 3 and 4 the kinematics of the stars of horizontal branch type appears to have a trend along the HB indeed.

The sdB stars have in general rather disk-like orbits and kinematical properties. The ones analysed here (Table 4) show the same behaviour as those from the large sample of sdB stars investigated previously (de Boer et al. 1997a).

The HB stars, the prime goal of our investigation, span a wide range in orbit parameters but when this group is split in HBB and HBA stars a cut is present.

The (hotter) HBB stars behave rather like the sdBs with orbits of disk-like characteristics. However, such stars are difficult to recognize and our sample is small. A much larger sample may show a larger variation in kinematics.

The HBA stars have mostly halo orbits (mean $\Theta \simeq 17$ km s$^{-1}$). This is very similar to the value at which most other studies concerning metal poor stars in the solar neighbourhood arrive (see Table 2 of Kinman 1995). However, the known sample may be observationally skewed toward stars with low atmospheric metallicity (large Balmer jump).

The RR-Lyrae stars have orbits spanning a large range in orbital parameters, too. However, a trend seems to be present with metallicity. The metal poor stars have halo orbits similar to those of the HBA stars with rather low orbital velocities of less than 100 km s$^{-1}$, and large $e$ and $\omega$. The metal rich stars on the other hand have rather disk-like kinematical characteristics. A similar distribution of metallicities and orbital velocities was also found in the studies of Chen (1999) and Martin & Morrison (1998).

Although there are a few RR Lyrae stars having high orbital velocities ($\Theta \geq 160$ km s$^{-1}$) and clearly disk-like orbits (some of which are very metal poor), HBA stars with such characteristics are not found in our sample. On the other hand no RR Lyraes with [Fe/H]$> -0.9$ dex with halo-like orbits or kinematics are present. This means that a high metallicity for a RR Lyr star is a good indicator that it is a disk star. However, a low metallicity does not mean that a star necessarily belongs to the halo.

For an overview of literature data on values for $\Theta$ (or asymmetric drift) for various star groups we refer to Fig. 3 in the review of Gilmore et al. (1989).

6.2. Discussion

Since the sdB stars (and possibly the HBB stars) have disk-like orbits, these stars must be a part of a relatively younger, more metal rich group among the HB stars. Majewski (1993) uses the expression ‘intermediate Population II’, other authors use the words ‘thick’ or ‘extended disk’. In addition to the disk-nature of their orbits, the vertical distribution is consistent with a scale height of the order of 1 kpc (Villeneuve et al. 1995, de Boer et al. 1997a).

Since the amount of metals in their atmospheres may have been altered by diffusion it is not possible to estimate the true age from the metallicity.

The HBA stars have really halo orbits. This must mean they belong to a very old population. Their atmospheric metal content is low indeed, the determinations showing a large scatter per star and from star to star ranging between $-1$ and $-2$ dex. However, metal rich HBA stars which are known to exist in star clusters (see Peterson & Green 1998), would likely be underrepresented in the sample.

If the halo contains mostly old stars, like globular cluster stars, then the resulting halo HB stars should occupy the HB in ranges related with metallicity as with the globular clusters (see Renzini 1983). The very metal poor ones ([M/H] $\simeq -2$ dex) would be HB stars of HBB and HBA nature as well as RR Lyrae, the ones of intermediate metallicity ([M/H] $\simeq -1.5$ dex) would be very blue down to sdB like, and the metal rich ones ([M/H] $\simeq -1$ dex) would be RHB stars, perhaps including some RR Lyrae. This behaviour may also explain the existence of the two Oosterhof groups (see van Albada & Baker 1973 or Lee et al. 1990) of RR Lyrae, since only the very metal poor and the relatively metal rich globular clusters contain RR Lyrae. Evolutionary changes of the HB stars may also affect the location on the HB (Sweigart 1987, Clement & Shelton 1999).

However, sdB stars with halo kinematics have not been found (de Boer et al. 1997a). Instead, they have only disk orbits. This must mean that the stars which originally formed in the halo had an initial mass, a metallicity and a red giant mass loss such that RR Lyrae and HBA stars were the end product, and not sdB stars.

As for the RR Lyrae stars, they show a wide range in kinematic behaviour, more or less in line with the atmospheric metal content. The actual metallicity did not bias the identification of these stars, since they are selected based on variability. One tends to divide the RR Lyrae sample into metal poor and metal rich RR Lyrae (see Layden 1994). Here we recall that in the HB stars the
contents of heavier elements in their atmospheres may be altered (see Sect. 1). The RR Lyrae stars with the continuous upheaval of the pulsation may stimulate mixing so that their atmospheres probably show the true metallicity. Thus, for RR Lyraes the metallicity may be used as a general population tracer. The observed range of metallicities would mean that there are old as well as younger RR Lyraes.

Old RR Lyrae must be very metal poor and should have halo orbits. The majority of the RR Lyrae included in our analysis fit these parameters. There are, however, a substantial number of RR Lyr stars in our sample with disk-like kinematics but low metallicities, in several cases as low as \(-2\) dex. The origin of this group of stars, dubbed the ‘metal weak thick disk’, is still unknown (see Martin & Morrison 1998 for a discussion).

Young (or younger) RR Lyrae should be relatively metal rich and have disk orbits. The investigated sample contains such stars. These objects should have an age, main-sequence mass, metallicity and RGB mass loss such that RR Lyrae emerge, i.e. HB stars with a thicker hydrogen shell. They are, being relatively metal rich, also of slightly different \(M_V\) than the metal poor and old ones. In fact, they are fainter and their distances should be based on the appropriate brightness-metallicity relation. The dependence is, however, feeble and amounts to just 0.1 mag for 0.5 dex. We tested how serious ignoring this effect is on the derived orbits by reducing the RR Lyr star distances by 10%. It does not lead to a change of significance in the histogram of Fig. 4.

6.3. Summary

Our orbit studies allow to see a trend in the kinematics of the field HB stars along the horizontal branch. This appears to give us access to the structure of the Milky Way and its halo as well as information about possible formation scenarios. The trends related with age and history could only be found using the kinematics, since it has become clear that the atmospheric metallicity in HB-like stars has no relation to the one of the main sequence progenitor. The location of the stars on the HB must be a complicated function of age, main-sequence mass, initial metallicity, and mass loss on the RGB. For the HB-like stars of today indications for the age can be determined from the present kinematic parameters. Only detailed models for metallicity dependent stellar evolution from main sequence through the RG phase with mass loss should, in comparison with the observables of horizontal branch stars, eventually be able to retrieve the true origin of the HB stars.

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