3/2 fractional quantum Hall plateau in confined two-dimensional electron gas

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Even-denominator fractional quantum Hall (FQH) states, such as 5/2 and 7/2, have been well known in a two-dimensional electron gas (2DEG) for decades and are still investigated as candidates of non-Abelian statistics. In this paper, we present the observation of a 3/2 FQH plateau in a single-layer 2DEG with lateral confinement at a bulk filling factor of 5/3. The 3/2 FQH plateau is quantized at $\frac{3}{2}\frac{e^2}{C_0C_1}$ within 0.02%, and can survive up to 300 mK. This even-denominator FQH plateau may imply intriguing edge structure and excitation in FQH system with lateral confinement. The observations in this work demonstrate that understanding the effect of the lateral confinement on the many-body system is critical in the pursuit of important theoretical proposals involving edge physics, such as the demonstration of non-Abelian statistics and the realization of braiding for fault-tolerant quantum computation.

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The fractional quantum Hall (FQH) effect has been investigated to extend our understanding of strongly interacting particles in two dimensions since its discovery. Most of the observed fractional states are odd-denominator states and can be explained under the framework of the composite fermion theory. For example, the 1/3 FQH state can be mapped into the filling factor $\nu = 1$ integer quantum Hall (IQH) state of composite fermions carrying fractional charge of $e/3$, which leads to a fractional $\frac{1}{3}$ Hall conductance. At half-filled $N = 0$ Landau level ($\nu = 1/2, 3/2$), the absence of FQH states is attributed to the formation of Fermi sea of composite fermions. The discovery of the first even-denominator state, the 5/2 FQH state, as viewed as a paired state of composite fermions with $e/4$ fractional charge, further enriched the knowledge of interacting electrons. Recent studies such as phase transition to the stripe phase, and even-denominator states in other two-dimensional systems, keep providing interesting physics at even-denominator filling factors.

The excitations in the FQH system carry fractional charge owing to the strong correlation between electrons. Besides, there is another equally famous way of charge fractionalization through topological soliton and topological phase transition, which is related to the boundary of a realistic experimental system. Theoretical treatments for the FQH effect usually consider an infinite 2DEG, but experiments can only measure finite samples with boundaries. The quantum Hall edge originating from the boundary was discussed and later described by chiral Luttinger liquids. Experiments based on the FQH edge physics have provided many exciting results and led to more efforts, such as the measurement of fractional charge, weak quasi-particle tunneling between edge currents and the search of the neutral modes. Theoretically, a 2DEG confined in an interferometer is proposed to test the non-Abelian statistics directly, and the interference of the edge current has been measured. Although the realistic boundary of a many-body system may complicate the theoretical treatment, the confinement can be a powerful experimental approach to manipulate the system. Even though the FQH effect has been studied for decades, systems of interacting electrons with confinement are still an open area for exploration.

Here we show an even-denominator FQH plateau quantized at $(\frac{5}{3})/20$ under lateral confinement in a single-layer 2DEG. This plateau develops below 300 mK with a quantization of 0.02%. The current transmitting through the confined region also causes a quantized two-terminal conductance at $\frac{1}{2}$, and a backscattered current induces a quantized tunneling conductance at $\frac{1}{5}$.

**Results**

**Gate-defined confinement.** The Hall bar samples were made from a wafer of GaAs/AlGaAs heterostructures. The 2DEG is about 200 nm below the sample surface. Two separate gates were deposited on the surface for the confined region. A sketch of the Hall bar and measurement setup are shown in Fig. 1a. The inset is an SEM picture of a device with the same gate geometry as that used in this experiment. The lithography dimension is $1 \times 2 \mu m^2$. The measurement of fractional charge, weak quasi-particle tunneling between edge currents and the search of the neutral modes.

![Sample information and the diagonal resistance and the Hall resistance traces.](image)

**Fig. 1** Sample information and the diagonal resistance and the Hall resistance traces. **a** A sketch of the Hall bar and the measurement setup. **b** Gate voltage dependence of the diagonal resistance $R_D$ at $B = 0$ T and $T = 6$ K. The inset is an SEM picture of a device with the same gate geometry as that used in this experiment. The lithography dimension is $1 \times 2 \mu m^2$. **c** The diagonal resistance and the Hall resistance traces with $V_{gate} = -4.5$ V at 18 mK. The black line is the Hall resistance $R_{XY}$ and the blue line is the diagonal resistance $R_D$. Both of them develop a series of IQH and FQH plateaus. $R_D$ was measured from contact 3 to contact 4, and $R_{XY}$ was from contact 6 to contact 5. Source data are provided as a Source Data file.
quantization of 0.02%, the resolution of this experiment. The 3/2 FQH plateau of \( R_D \) and the 5/3 FQH plateau of \( R_{XY} \) center at almost the same magnetic field, and the width of these two plateaus are similar at 18 mK. Analogous to conventional FQH states, the width of the 3/2 plateau decreases with increasing temperature. Interestingly, the 3/2 FQH plateau is even wider than that of the 5/3 FQH plateau at 100 mK (Fig. 2b), and the 3/2 FQH plateau can survive up to 300 mK (Supplementary Fig. 1), which indicates that the 3/2 plateau is more stable than all the previously observed even-denominator FQH plateaus in a single-layer 2DEG. The observation of such a 3/2 FQH plateau has been reproduced in different samples with different device sizes (see Supplementary Note 1).

The critical parameter to trigger the appearance of the 3/2 FQH plateau is the gate voltage. The diagonal resistance traces with different gate voltages at 18 mK are shown in Fig. 3a. The diagonal resistance develops the 5/3 FQH plateau with \( V_{\text{gate}} = -2.8 \) V, and becomes larger with less negative gate voltage. When the gate voltage is less negative than or equal to \(-2.0 \) V, the 3/2 FQH plateau appears. The gate voltage dependence of the 3/2 FQH plateau can also be demonstrated by the relationship between the gate voltage and the diagonal resistance. As shown in Fig. 3b, the diagonal resistance changes from \((\frac{3}{2})/\frac{1}{2}\) to \((\frac{3}{2})/\frac{1}{2}\) when the gate voltage is swept from \(-1.3 \) V to \(-3.0 \) V at the magnetic field of 7.67T, near the center of the 5/3 FQH plateau in the bulk. At the same time, the Hall resistance is consistently quantized at \((\frac{3}{2})/\frac{1}{2}\), indicating the 5/3 FQH state in the bulk of the Hall bar is not influenced by the gate voltage.

Another essential condition for the observation of the 3/2 FQH plateau is the gate annealing procedure with appropriate negative gate voltage. In our samples, \( V_{\text{gate}} = -1.3 \) V is sufficient for the depletion of the electrons underneath the gates, as shown in Fig. 1b and Fig. 3c. During the measurements for the 3/2 FQH plateaus in Fig. 2, Fig. 3a, b, we did the annealing procedure with \( V_{\text{gate}} = -4.5 \) V. If the gates are annealed at \(-1.5 \) V, even though enough to achieve the confined region, the 3/2 FQH plateau will not appear (Supplementary Fig. 2).

In order to demonstrate the full depletion underneath the confinement gates, we fabricated a sample with a single top gate crossing the entire Hall bar. This gate was also annealed at \( V_{\text{gate}} = -4.5 \) V, and the measurement was carried out at bulk filling factor 5/3 and \( T = 18 \) mK. As shown in Fig. 3c, the conductance across the top gate is always zero when the gate voltage is more negative than \(-1.25 \) V. In another sample, we fabricated an individual gate (defined as arm gate in Fig. 3d) next to the confined region. As shown in Fig. 3d, a small negative gate voltage on this arm gate, far away from depleting values, is enough to break the 3/2 FQH plateau. These two control experiments demonstrated that the 3/2 FQH plateau is induced by the confined region.

In the confined region, a possible result caused by the annealing procedure and gate voltage change is quasi-particle tunneling. When \( V_{\text{gate}} = -4.5 \) V is applied to the gates, the electrons both underneath and around the gates will be depleted. The annealing procedure may adjust the charge distribution of the donor layer at \( T > 4 \) K, which causes a very sharp potential in the confined region at the measurement temperature range, and supports the 5/3 FQH state in the confined region (Fig. 1c). When the gate voltage is changed to less negative values, such as \(-2.0 \) V in Fig. 3a, at the lower temperature, the effective residual potential from both the gates and the donor layer may generate some disorders to the 2DEG, which facilitate the quasi-particle tunneling between the counter-propagating edge states in the confined region. More negative annealing gate voltage and less negative measurement gate voltage will generate more disorders.

**Source Data.** Source data are provided as a Source Data file.

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**Four-terminal resistance.** In our samples, the confined region is formed and controlled by the gate voltages. Changing the gate voltage will tune the lateral confinement but not influence the bulk properties. As shown in Fig. 2a, when the gate voltage is changed to \(-1.3 \) V, the Hall resistance \( R_{XY} \) does not change. Unexpectedly, the diagonal resistance \( R_D \) develops an even-denominator FQH plateau quantized at \((\frac{3}{2})/\frac{1}{2}\), with a
resulting in stronger quasi-particle tunneling. Strictly, the diagonal resistance is the sum of the Hall resistance in the bulk of the Hall bar and the tunneling resistance in the confined region. As a result, the variation of the diagonal resistance may be caused by the quasi-particle tunneling.

Two-terminal conductance. From the Landauer-Büttiker theory, when the diagonal resistance develops the 3/2 FQH plateau, the conductance \( \frac{e^2}{h} \) will transmit through the confined region, which has been verified in our measurements. Fig. 4a shows the two-terminal conductance traces at 18 mK. At filling factor 5/3, the conductance is quantized at \( \frac{5e^2}{h} \) with \( V_{\text{gate}} = -2.8 \) V and at \( \frac{4e^2}{h} \) with \( V_{\text{gate}} = -1.3 \) V. The conductance in the bulk of the Hall bar should be \( \frac{3e^2}{h} \) at filling factor 5/3. When the conductance transmitting the confined region is \( \frac{3e^2}{h} \), the tunneling conductance will be \( \frac{1e^2}{h} \). The corresponding propagating edge channels are sketched in Fig. 4b, where the dashed lines represent the tunneling conductance quantized at \( \frac{2e^2}{h} \). This edge channel picture has also been verified by four-terminal resistance and two-terminal conductance measurements with the reversed magnetic field (Supplementary Figs. 4 and 5).

Discussion
In general, the density of the gate-defined confinement region is smaller than that of the bulk, and affected by the gate voltage. However, the gate annealing procedure can keep uniform density for the whole sample in our measurements. This can be verified by the magnetic field dependence of the IQH and FQH plateaus in Hall traces in Fig. 1c and Supplementary Fig. 6. By comparing the diagonal resistance and the Hall resistance as a function of magnetic field for the gating condition of developing the 3/2 FQH plateau (Fig. 3a), the 3/2 plateau in this measurement appears at the filling factor of 5/3. What’s more, if the density of the confinement is reduced to filling factor 3/2 when the 3/2 plateau shows up at \( -1.8 \) V (Fig. 3a), then further negatively charging the top gate will only maintain or keep reducing the density in the confinement. As a result, the 5/3 plateau could not show up anymore at the filling...
factor 3/2 or at a smaller filling factor, which is contradicted to the experimental observation (−2.8 V at Fig. 3a). This argument serves as an additional clue that the 3/2 FQH plateau appears at the filling factor of 5/3. The 3/2 FQH plateau has also been observed in Charles M. Marcus group, shown in Yiming Zhang’s thesis. In their measurements, the 3/2 FQH plateau appeared in samples with both uniform density and non-uniform density. From the corresponding R-B features between $R_D$ and $R_{XY}$ in Fig. 1c and Supplementary Fig. 6, the 3/2 FQH plateau we observed is unlikely induced only by the density variation in the confined region.

Disorder can drive the collapse of energy gap and then induce phase transition from the FQH state to another state. At $v = 5/3$ FQH state, the edge state could be complicated due to potential edge reconstruction and neutral mode. The formation of the 3/2 FQH plateau could be caused by a more complicated edge reconstruction with lateral confinement at $v = 5/3$. In our system, the disorders induced by the residual potential in the confined region could also help with the collapse of the 5/3 FQH state and the formation of intriguing edge structure and excitation with fractional charge. The 3/2 FQH plateau has been found in the single-layer two-dimensional system of ZnO where Landau level crossing induced by tilted magnetic field is needed.

while there is no in-plane magnetic field in our measurements. The exact origin of the 3/2 FQH plateau remains an open theoretical question to be investigated.

**Methods**

**Sample fabrication.** The samples were made from a wafer of GaAs/AlGaAs heterostructures. The center of the 30 nm quantum well is 210 nm below the surface, with modulated Si doping at ~100 nm below and above the quantum well center. The mobility is higher than $1.0 \times 10^7 \text{cm}^2 \text{V}^{-1} \text{s}^{-1}$ at 20 mK. A 150 µm wide Hall bar was shaped by wet etching. Ohmic contacts were made of Pt/Au/Ge alloy deposited by e-beam evaporation and annealed at 550 °C for 100 s. Two separate Cr/Au gates were deposited on the surface of the sample to form the confined region. In this experiment, samples with different confined region sizes were fabricated and measured. The dimensions of these geometries are $1 \times 2 \mu m^2$, $0.3 \times 2 \mu m^2$, and $1.5 \times 3 \mu m^2$, respectively. The confined region on the samples used in the main text is the size of $1 \times 2 \mu m^2$. The data from other samples are shown in the Supplementary Figs. 1–3.

**Measurement techniques.** The measurements were carried out in a dilution refrigerator with a base refrigerator temperature below 6 mK. The temperatures given in this work are electron temperatures. In the four-terminal resistance measurements, the Hall resistance $R_{XY}$ and the diagonal resistance $R_D$ were measured simultaneously using lock-in techniques at 6.47 Hz with 1 nA. The two-terminal conductance measurements were also carried out using lock-in techniques at 6.47 Hz with voltage excitations smaller than 35 µV.

**Data availability**
The authors declare that the main data supporting the findings of this study are available within the article and its Supplementary Materials. Extra data are available from the corresponding author upon request. The source data underlying Figs. 1b, c, 2, 3, 4a and Supplementary Figs. 1–6 are provided as a Source Data file.

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Author contributions

H.F., R.Z., J.S., P.S., and P.W. performed the measurements. H.F. and R.Z. fabricated the devices. L.N.P. and K.W.W. prepared and supplied the GaAs wafer. H.F. and X.L. initiated the research. H.F., R.Z., J.S., Z.Z., P.W., and X.L. analyzed the results. Y.W., H.L. and X.C.X. provided the theoretical attempt. H.F., Y.W., H.L., X.C.X., and X.L. discussed the results and wrote the paper.

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