High-Precision Cutting Edge Radius Measurement of Single Point Diamond Tools Using an Atomic Force Microscope and a Reverse Cutting Edge Artifact

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Abstract: This paper presents a measurement method for high-precision cutting edge radius of single point diamond tools using an atomic force microscope (AFM) and a reverse cutting edge artifact based on the edge reversal method. Reverse cutting edge artifact is fabricated by indenting a diamond tool into a soft metal workpiece with the bisector of the included angle between the tool’s rake face and clearance face perpendicular to the workpiece surface on a newly designed nanoindentation system. An AFM is applied to measure the topographies of the actual and the reverse diamond tool cutting edges. With the proposed edge reversal method, a cutting edge radius can be accurately evaluated based on two AFM topographies, from which the convolution effect of the AFM tip can be reduced. The accuracy of the measurement of cutting edge radius is significantly influenced by the geometric accuracy of reverse cutting edge artifact in the proposed measurement method. In the nanoindentation system, the system operation is optimized for achieving high-precision control of the indentation depth of reverse cutting edFigurege artifact. The influence of elastic recovery and the AFM cantilever tip radius on the accuracy of cutting edge radius measurement are investigated. Diamond tools with different nose radii are also measured. The reliability and capability of the proposed measurement method for cutting edge radius and the designed nanoindentation system are demonstrated through a series of experiments.

Keywords: single point diamond tool; cutting edge radius; reversal method; nanoindentation system; elastic recovery

1. Introduction

Ultra-precision diamond cutting, combining a single point diamond tool with an ultra-precision lathe, has been widely employed for the fabrication of microstructure elements, such as microlens arrays [1], compound eye freeform surfaces [2], and sinusoidal grids [3,4]. The achievable machining accuracy of the ultra-precision diamond cutting is significantly affected by the geometry of the diamond tool, including cutting edge contour, cutting edge radius, and tool faces [5–7]. In order to achieve a nanometric machining accuracy, it is essential to conduct a quantitative evaluation of the geometry of the diamond tool, especially cutting edge radius, which determines the minimum depth of cut and the surface finish of the machined microstructures [8,9].

Cutting edge radius of a diamond tool is usually required to be within 10 to 100 nm for ultra-precision diamond cutting [10]. Therefore, the methods for cutting edge radius measurement
should have a nanometric measurement accuracy in both lateral and vertical directions [11]. Optical methods can conduct fast and non-contact measurements [12–14]. However, a lateral resolution that is larger than 10 nm is limited by the optical diffraction phenomenon which occurs around the cutting edge when an optical method is used to measure the geometry of the diamond tool. Scanning electron microscopes (SEMs) have a nanometric lateral resolution and a wide view field [15]. However, because SEMs have a limitation of two-dimensional (2D) projection, they can only be used for the qualitative evaluation of diamond tool cutting edge radius and cannot be used for the quantitative evaluation. In addition, the material of diamond tools also influences the measurement accuracy of the diamond tool cutting edge radius using SEMs [16]. Atomic force microscopes (AFMs), which can provide a three-dimensional (3D) measurement with a nanometric accuracy in both lateral and vertical directions, can directly measure the diamond tool cutting edge radius by accurately aligning the AFM cantilever tip with the diamond tool cutting edge within the measurement range of the AFM [17–19]. However, the process for an accurate alignment is extremely time-consuming and the AFM cantilever tip can also be easily damaged due to an inaccurate alignment operation.

An indirect measurement method based on an AFM has been proposed to address the above problems using an AFM to measure cutting edge radius of a diamond tool [20]. A profile of a diamond tool cutting edge is copied on a copper workpiece by indenting the diamond tool into the workpiece on an ultra-precision lathe. Then, the copied profile is scanned by an AFM, from which the diamond tool cutting edge radius can be obtained. Since this indirect measurement method can protect the diamond tool and the AFM cantilever tip from damage, and also shorten the measurement time, it is attractive for practical applications. However, the elastic recovery of the copied profile can affect the measurement accuracy, which is not considered in the indirect measurement method based on the AFM. More importantly, since both the direct and indirect measurement methods are based on an AFM, the obtained profile is a geometric convolution of the AFM tip and the actual and copied diamond tool cutting edges. It is essential to eliminate the convolution effect of the AFM tip whose size is comparable to that of the diamond tool cutting edge, for achieving a high-precision diamond tool cutting edge radius measurement.

There are two approaches for reducing the convolution effect of the AFM tip. One approach is to directly characterize the AFM tip with a form surface measuring instrument. The other is to make an error separation operation on the AFM images for removing the influence of the AFM tip profile. Compared with the direct characterization approach, the error separation approach is more effective because no additional form surface measuring instruments are necessary [21]. An edge reversal error separation method based on an AFM was proposed for measuring cutting edge radius of diamond tool without the effect of the AFM tip radius by the authors of [22]. Firstly, a replicated cutting edge was obtained by indenting a diamond tool into a soft metal material. Then, an AFM was applied to scan the actual and the replicated cutting edges. The cutting edge radius of the diamond tool was obtained by taking the difference between the AFM images of the actual and the replicated cutting edges when the elastic recovery of the replicated cutting edge was small as compared with the cutting edge radius. Molecular dynamics (MD) simulations were carried out to investigate the effect of elastic recovery on cutting edge radius in our previous researches [23,24]. It was verified that when the indentation depth of the replicated cutting edge was set to be larger than 200 nm, the elastic recovery of the replicated cutting edge could be ignored. However, a large indentation depth would cause more measurement uncertainties in the AFM measurement of the replicated tool cutting edge.

Meanwhile, a nanoindentation instrument has been designed for replicating the diamond tool cutting edge onto a soft workpiece surface [25]. The displacement of the diamond tool was monitored by a capacitive sensor of a fast tool servo (FTS) unit, which was employed to drive the diamond tool. The workpiece was pasted on a cantilever whose deflection was detected by another capacitive sensor. The indentation depth of the diamond tool was obtained from the outputs of the two capacitive sensors. However, it was a time-consuming process to replicate the diamond tool cutting edge using this nanoindentation instrument. In addition, a contact damage would be generated on the workpiece
surface when the tool-workpiece contact was established before the replication. The contact damage would influence the indentation depth and the profile of the replicated cutting edge.

In this paper, we present high-precision cutting edge radius measurements of single point diamond tools using an AFM and a reverse cutting edge artifact based on the proposed edge reversal method and the designed nanoindentation system. After introducing the measurement principles, the operation of the nanoindentation system is optimized for achieving high-precision control of the indentation depth. The effects of the elastic recovery and the AFM cantilever tip on the measurement accuracy and the measurement uncertainty are investigated. A series of experiments are preformed to verify the reliability and the capability of the proposed method and the designed system.

2. Principle of Measuring Cutting Edge Radius

There are three steps in the process of measuring the diamond tool cutting edge radius using the proposed edge reversal method, as shown in Figure 1.

![Figure 1. Principle of the proposed edge reversal method.](image)

The first step is related to the cutting-edge replication shown in Figure 1. The single point diamond tool, a piece of copper workpiece, and a nanoindentation system are employed. An indentation mark, referred to as the reverse cutting edge artifact, is fabricated by indenting the diamond tool into the workpiece with the bisector of the included angle between its rake face and clearance face perpendicular to the workpiece surface using the nanoindentation system. The configuration and the principle of the nanoindentation system is introduced later. The reverse cutting edge artifact is, thus, directly transcribed from the geometry of the diamond tool.

The second step is related to the AFM measurement of the actual cutting edge of the diamond tool. The diamond tool, with the cutting edge radius, \( R_{\text{tool}} \), is positioned under the AFM cantilever with the bisector of the included angle between its rake face and clearance face along the vertical axis. An AFM cantilever is moved by an XY-stage and a Z-scanner of the AFM along the X-, Y-, and Z-directions to align the AFM cantilever tip with the apex of the diamond tool cutting edge. After an accurate alignment, the AFM cantilever is brought to scan across the diamond tool cutting edge. Since the tip radius \( R_{\text{tip}} \) of the AFM cantilever is comparable to the cutting edge radius, \( R_{\text{tool}} \), of the diamond tool, the scan trace of the AFM with an apex radius of \( R_{\text{tool_m}} \) is a convolution of the AFM tip and the diamond tool cutting edge, as shown in Figure 1. Therefore, the following equation can be obtained:

\[
R_{\text{tool_m}} = R_{\text{tool}} + R_{\text{tip}}
\]
The third step is related to the AFM measurement of the reverse cutting edge artifact. Then, the reverse cutting edge artifact is measured by the AFM. The apex radius of the reverse cutting edge is defined as $R_{\text{mark}}$, which is also comparable to the AFM tip radius $R_{\text{tip}}$. After the alignment between the AFM cantilever tip and the apex of reverse cutting edge, the AFM tip scans across the reverse cutting edge artifact to map out its topography. The scanned image is also a convolution of the AFM tip and the reverse cutting edge artifact. Therefore, the following equation can be obtained:

$$R_{\text{mark,m}} = R_{\text{mark}} - R_{\text{tip}}$$  \hspace{1cm} (2)

The copper workpiece surface displays a certain degree of elastic recovery after the diamond tool is withdrawn from the surface in the nanoindentation process [23,24]. The relationship between the actual cutting edge radius and reverse cutting edge radius can be expressed as:

$$R_{\text{tool}} = (1 - \xi)R_{\text{mark}}$$  \hspace{1cm} (3)

where $\xi$ represents the elastic recovery coefficient of the reverse cutting edge artifact. According to Equations (1)–(3), cutting edge radius of the diamond tool can be evaluated to be:

$$R_{\text{tool}} = \frac{1}{2 - \xi} (R_{\text{tool,m}} + R_{\text{mark,m}})$$  \hspace{1cm} (4)

Therefore, cutting edge radius of the diamond tool can be obtained without being influenced by the AFM tip radius. As can be seen from Equation (4), the achievable accuracy of this method depends on the elastic recovery coefficient $\xi$. It has been verified that the elastic recovery coefficient, $\xi$, of the reverse cutting edge would be reduced to 0.012 from 0.068 when the indentation depth was increased to 20 nm from 2.5 nm based on molecular dynamics (MD) simulations [22]. The detail of the MD simulation can be found in [22] and is not repeated in this paper for the sake of clarity. The difference between $R_{\text{mark}}$ and $R_{\text{tool}}$ was evaluated to be 0.24 nm when the indentation depth was set to be 200 nm. The difference is small and is negligible for the cutting edge radius measurement as compared with the cutting edge radius. However, when the indentation depth is set to be 200 nm, the measurement uncertainty in the tool cutting edge radius measurement becomes large. Therefore, the indentation depth should be controlled within a range of 20 to 200 nm.

A nanoindentation system is, then, designed for achieving the requirement of high-precision indentation depth control of the reverse cutting edge artifact as shown in Figure 2. A single point diamond tool is mounted on the FTS to indent into a prepolished metal workpiece by a linear stage and/or the FTS. When the distance between the diamond tool tip and the workpiece surface is larger than the motion stroke of the FTS, the linear stage is employed to move the diamond tool to approach the workpiece surface by a steeping motor controller. The displacement of the diamond tool driven by the linear stage and the FTS can be measured by the linear encoder of the stage and the displacement sensor of the FTS unit (inside sensor). The workpiece is attached on a cantilever. One end of the cantilever is fixed on a holder and the other end is preloaded by a preload controller. An outside displacement sensor (outside sensor) is used to detect the deflection of the cantilever caused by the indentation. Two XY-manual stages (Stage 1 and Stage 2) are used for the alignment between the workpiece surface and the diamond tool tip. The outputs of two sensors are collected by an oscilloscope for further evaluating the indentation depth $d_{\text{depth}}$ based on the following equation:

$$d_{\text{depth}} = d_{\text{in}} - d_{\text{out}}$$  \hspace{1cm} (5)

where $d_{\text{in}}$ and $d_{\text{out}}$ represent the outputs of the inside and the outside sensors, respectively.
Figure 2. Schematic of the nanoindentation system.

The operation of the nanoindentation system is optimized for achieving high-precision control of the indentation depth during the tool cutting edge replication, as shown in Figure 3. There are three steps for replicating the cutting-edge geometry of a diamond tool into a workpiece surface. In step one, the linear stage is firstly used to move the diamond tool to the initial position shown in Figure 3a, where the distance between the diamond tool tip and the workpiece surface is equal to the motion stroke of the FTS. Then, the diamond tool is actuated by the FTS with a step of 5 nm to avoid any unexpected contact damages on the workpiece surface. The output of the outside sensor does not change in this step, as shown in Figure 3b. In step two, the contact between the diamond tool and the workpiece is established at the contact position where the output of the outside sensor starts to vary due to the deflection of the cantilever. A small indentation mark with a depth less than 5 nm is generated on the workpiece surface, which is small as compared with the reverse cutting edge. Therefore, the effect of the small indentation mark can be ignored. In step three, the diamond tool is indented into the workpiece surface with the command indentation depth, which can be evaluated by substituting the outputs of two sensors at the indentation position into Equation (5). Therefore, a reverse cutting edge artifact with a high-precision depth is fabricated by following these three steps.

Figure 3. Cont.
The copper workpiece was pasted on an aluminum cantilever with a spring constant of 155 N/m. The workpiece surface was smooth enough for replicating the diamond tool cutting edge geometry.

A series of experiments were performed to investigate the effect of elastic recovery on the reverse cutting edge artifact and the AFM cantilever tip on the measurement accuracy of the cutting edge radius as well as to verify the reliability of the proposed edge reversal method and the capability of the designed nanoindentation system.

Since copper has a relatively large Young’s modulus, a prepolished copper workpiece with a size of 10 mm (length) × 10 mm (width) × 2 mm (thickness) was selected as the workpiece. Figure 4a shows the topography of the copper workpiece surface measured by a commercial AFM (Innova, Bruker, Billerica, MA, USA). As shown in Figure 4b, the Root Mean Square (RMS) roughness of the section A–A’ of the copper workpiece was evaluated to be 2.43 nm based on a 3D AFM topography. The workpiece surface was smooth enough for replicating the diamond tool cutting edge geometry.

The copper workpiece was pasted on an aluminum cantilever with a spring constant of 155 N/m at the contact point. The deformation of the aluminum cantilever was detected by a capacitive sensor (6800, MicroSense, Lowell, MA, USA).

3. Experiment and Discussion

A series of experiments were performed to investigate the effect of elastic recovery on the reverse cutting edge artifact and the AFM cantilever tip on the measurement accuracy of the cutting edge radius as well as to verify the reliability of the proposed edge reversal method and the capability of the designed nanoindentation system.

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3.1. Effect of Elastic Recovery

The effect of elastic recovery of the reverse cutting edge artifact on cutting edge radius measurement accuracy was analyzed. An AFM cantilever (OMCL-AC240TS, Olympus, Tokyo, Japan) with a nominal tip radius of 7 nm and a tip height of 14 μm was selected to measure the topographies of the actual and the reverse diamond tool cutting edge. A single point diamond tool with a nose radius of 1 mm was measured in this test.
Since the indentation depth and the elastic recovery of the reverse cutting edge artifact are related with each other based on the Hertz theory, a group of reverse cutting edge artifacts with various indentation depths from 20 to 180 nm were fabricated on the designed nanoindentation system in order to investigate the effect of the elastic recovery. The interval of indentation depth was set at approximately 20 nm.

Figure 5 shows the outputs of the inside and the outside sensors when the command displacement of the diamond tool actuated by the FTS was set at 50 nm. Only the outputs in step three of Figure 3 are plotted in Figure 5. The output of the inside sensor was 52 nm, which was approximately the same as the command displacement of the diamond tool. The output of the outside sensor was 27 nm. The indentation depth of the reverse cutting edge artifact was calculated to be 25 nm by substituting the outputs of two sensors into Equation (5).

![Figure 5](image_url)  
*Figure 5. The outputs of the inside and the outside sensors with a command displacement of 50 nm.*

The diamond tool was positioned on the Z-scanner of the AFM with the bisector of the included angle between its rake face and clearance face. The Olympus AFM cantilever was moved along the X-, Y- and Z-directions by the XY-stage and the Z-scanner of the AFM to make the alignment between the AFM tip and the apex of the diamond tool cutting edge. The actual cutting edge was, then, scanned by the AFM cantilever. The scan range and the scan rate were set to be 2 \( \mu m \) \((X) \times 2 \mu m \) \((Y)\) and 1.2 \( \mu m/s \), respectively. The numbers of scanning lines in the X- and Y-positions were 1024 and 1024, respectively. Figure 6a shows a 3D topography of the diamond tool cutting edge. It can be seen from the figure that there was a clear edge between the rake face and the clearance face, which can be employed for quantitative evaluation of the diamond tool cutting edge radius. The cross-sectional profile extracted from the 3D topography is shown in Figure 6b. The measured tool cutting edge radius was obtained from that of the fitted arc, which was evaluated by fitting the points in the apex of the cross-sectional profile of the cutting edge based on the least square method. The radius of the fitted arc, referred to as \( R_{tool,m} \), was evaluated to be approximately 40.32 nm. It should be noted that the fitted arc was a geometric convolution of the AFM tip and the actual diamond tool cutting edge. Therefore, the value of 40.32 nm was not the actual diamond tool cutting edge radius.
The reverse cutting edge artifact was also placed on the Z-scanner of the AFM. The same AFM cantilever, which had been used to scan the actual cutting edge, was brought to scan the reverse cutting edge. The scanning range, the scan rate, and the number of scanning lines in the X- and Y-position were set to be the same as those in the AFM measurement of the actual cutting edge. Figure 7a,b shows the AFM topography and the cross-sectional profile of the reverse cutting edge artifact, respectively. It can be seen from Figure 7a that the reverse cutting edge was well transcribed from the geometry of the diamond tool. The depth of the reverse cutting edge artifact was evaluated to be 28 nm. It was approximately the same as the indentation depth of 25 nm, which was evaluated based on the outputs of the inside and the outside sensors of the nanoindentation system. The control accuracy of the indentation depth in the designed nanoindentation system was, therefore, verified from the result. The points in the apex of the measured revered cutting edge were fitted using the least square method, as shown in Figure 7b. The radius of the reverse fitted arc, referred to as \( R_{\text{mark}_m} \), was evaluated to be 21.04 nm. Similarly, the reverse fitted arc was a geometric convolution of the AFM tip and the reverse cutting edge. The value of 21.04 nm was not the reverse diamond tool cutting edge radius. Assuming \( \xi \) is equal to zero, the actual cutting edge radius, \( R_{\text{tool}} \), was calculated by substituting the evaluated \( R_{\text{tool}_m} \) and \( R_{\text{mark}_m} \) into Equation (4) to obtain 30.68 nm. The difference between \( R_{\text{tool}} \) and \( R_{\text{tool}_m} \) was evaluated to be 9.64 nm, which was close to the nominal AFM tip radius of 7 nm. On the basis of the experimental results, the effectiveness of the proposed measurement method for cutting edge radius using an AFM and a reverse cutting edge artifact was verified.

\[ R_{\text{mark}_m} = \frac{1}{2} \left( R_{\text{tool}_m}^2 + R_{\text{tool}_m} R_{\text{mark}_m} + R_{\text{mark}_m}^2 \right)^{1/2} \]

\( R_{\text{tool}_m} \) of other reverse cutting edges with various indentation depths were also evaluated using the proposed measurement method for cutting edge radius. The evaluated \( R_{\text{mark}_m} \) and \( R_{\text{tool}} \) are
The values were employed to evaluate the measurement uncertainty induced by the elastic recovery. As can be seen in the figure, the average diamond tool cutting edge radius was estimated to be 30.38 nm with a standard deviation of 0.31 nm. Therefore, it was verified that the elastic recovery of the reverse cutting edge artifact did not affect the measurement accuracy of cutting edge radius when the indentation depth was within 20 to 200 nm.

![Figure 8. Experimental results under various indentation depths.](image)

In addition, the effect of elastic recovery on measurement uncertainty of cutting edge radius was investigated. The indentation area between the diamond tool cutting edge and the workpiece, shown in Figure 9, can be recognized as a cylinder and a plane surface. According to the Hertz theory [26], for a plane surface and a cylinder with a radius of \( R_{\text{tool}} \), the elastic recovery \( d_{er} \) of the reverse cutting edge along the X-direction can be expressed by the following equation:

\[
d_{er} = 4 \frac{1}{\pi} \frac{1}{L} \frac{F}{E} \left(1 - \frac{v^2}{E}ight)
\]

where \( F \) is the applied indentation force between the diamond tool and the workpiece, which can be obtained from the deflection of the cantilever at the indentation position and the spring constants of the cantilever in the designed nanoindentation system. \( L \) is the length of cylinder, which can be obtained based on the indentation depth and the nose radius of the diamond tool. \( E \) and \( v \) represent the Young’s modulus and the Poisson’s ratio of the diamond tool, respectively.

![Figure 9. Schematic of the indentation area between the diamond tool and the copper workpiece.](image)

Figure 10 shows the elastic recovery of the reverse cutting edge under various indentation depths. The values were employed to evaluate the measurement uncertainty induced by the elastic recovery. The measurement uncertainty of cutting edge radius of a diamond tool with 1 mm nose radius was evaluated based on the Guide to the Uncertainty in Measurement (GUM) [27].
The standard deviation of the evaluated uncertainties was calculated to be 0.005 nm. The results further demonstrated that elastic recovery of the reverse cutting edge did not influence the measurement accuracy of the diamond tool cutting edge radius based on the proposed edge reversal method and the designed nanoindentation system.

The measurement uncertainties under various indentation depths are shown in Figure 11. The standard deviation of the evaluated uncertainties was calculated to be 0.005 nm. The results further demonstrated that elastic recovery of the reverse cutting edge did not influence the measurement accuracy of the diamond tool cutting edge radius based on the proposed edge reversal method and the designed nanoindentation system.

Table 1 shows the calculated uncertainties when the indentation depth was equal to 25 nm. The uncertainty in \( R_{\text{tool, } m} \) and \( R_{\text{mark, } m} \) was evaluated to be 1.36 and 1.42 nm, respectively. The uncertainty with a coverage factor of \( k = 2 \) (95% confidence) in the measurement of the diamond tool cutting edge radius was evaluated to be 1.97 nm, which was smaller than that obtained in our previous research [22].

The uncertainty in \( R \) was evaluated based on the Guide to the Uncertainty in Measurement (GUM) [27].

![Figure 10](image-url.png)

**Figure 10.** The theoretical elastic recovery under various indentation depths.

Table 1 shows the calculated uncertainties when the indentation depth was equal to 25 nm. The measurement uncertainties under various indentation depths are shown in Figure 11. The standard deviation of the evaluated uncertainties was calculated to be 0.005 nm. The results further demonstrated that elastic recovery of the reverse cutting edge did not influence the measurement accuracy of the diamond tool cutting edge radius based on the proposed edge reversal method and the designed nanoindentation system.

**Table 1.** Uncertainty analysis in the measurement of a diamond tool with a nose radius of 1 mm.

| Uncertainty Sources          | Symbol         | Uncertainty Value | Distribution | Standard Uncertainty |
|-----------------------------|----------------|-------------------|--------------|----------------------|
| Lateral imaging resolution  | \( u_L \)      | 0.97 nm           | Rectangular  | 0.56 nm              |
| Lateral positioning resolution | \( u_{L,n} \) | 1.2 nm            | Normal       | 1.2 nm               |
| Vertical positioning resolution | \( u_V \)   | 0.2 nm            | Normal       | 0.2 nm               |
| Thermal resolution          | \( u_t \)      | \( 3.3 \times 10^{-5} \) nm | Rectangular | \( 1.9 \times 10^{-5} \) nm |
| Measurement resolution      | \( u_d \)      | 1.457 nm          | -            | 0.46 nm              |
| Uncertainty in \( R_{\text{tool, } m} \) | \( u_{\text{tool, } m} \) | -                  | -            | 1.36 nm              |
| Lateral imaging resolution  | \( u_r \)      | 0.97 nm           | Rectangular  | 0.56 nm              |
| Lateral positioning resolution | \( u_{l,n} \) | 1.2 nm            | Normal       | 1.2 nm               |
| Vertical positioning resolution | \( u_{V,n} \) | 0.2 nm            | Normal       | 0.2 nm               |
| Thermal resolution          | \( u_{t,m} \)  | \( 4.9 \times 10^{-5} \) nm | Rectangular | \( 2.8 \times 10^{-5} \) nm |
| Measurement resolution      | \( u_{d,m} \)  | 0.385 nm          | -            | 0.12 nm              |
| Elastic recovery            | \( u_{e,m} \)  | 0.358 nm          | Rectangular  | 0.21 nm              |
| Indentation force           | \( u_{f,m} \)  | 0.001 nm          | Rectangular  | \( 5.7 \times 10^{-4} \) nm |
| Uncertainty in \( R_{\text{mark, } m} \) | \( u_{\text{mark, } m} \) | -                  | -            | 1.42 nm              |
3.2. Effect of AFM Cantilever Tip

The AFM cantilever was one of the crucial factors that affected the evaluation accuracy of the diamond tool cutting edge radius. Therefore, another AFM cantilever (MPP-11100-10, Bruker, Billerica, MA, USA) was installed onto the AFM to scan the actual and the reverse diamond tool cutting edges for investigating the effect of the AFM cantilever tip on the measurement accuracy of the diamond tool cutting edge radius. The Olympus AFM cantilever and the Bruker AFM cantilever were referred to as Cantilever 1 and Cantilever 2, respectively. Differing from Cantilever 1, there was a long base at the top of Cantilever 2. The tip radius of Cantilever 2 was 12 nm, which was larger than that of Cantilever 1.

Then, Cantilever 2 was used to scan the actual and the reverse cutting edges, which had been scanned by Cantilever 1. We confirmed that the AFM topographies of the cutting edges scanned by Cantilever 2 were similar to those measured by Cantilever 1, although the AFM images are not shown here for the sake of clarity. Figure 12 shows the measured diamond tool cutting edge radii using Cantilever 2. The average characterized cutting edge radius of the diamond tool was 29.67 nm, with a standard deviation of 0.16 nm. Characterized cutting edge radius using Cantilever 2 was the same as that using Cantilever 1. The measurement uncertainty using Cantilever 2 was evaluated. The results are also plotted in Figure 12. The standard deviation of the evaluated uncertainty values was calculated to be 0.028 nm. From the above results, it can be seen that the measurement accuracy of the diamond tool cutting edge radius based on the proposed edge reversal method was not affected by the AFM cantilever tip radius. This is consistent with the fact that the effect of the AFM cantilever tip radius can be removed in the proposed method.

Figure 11. The measurement uncertainties of cutting edge radius of a diamond tool under various indentation depths.

Figure 12. Experimental results using Cantilever 2.
3.3. Reliability of the Proposed Method and the Designed System

To further demonstrate the reliability of the proposed measurement method, cutting edge radius of a diamond tool with a different nose radius of 2 mm, which was referred to as Diamond Tool 2, was also evaluated.

Diamond Tool 2 was mounted on the nanoindentation system to replicate its cutting edge on the copper workpiece with various indentation depths. The AFM with Cantilever 1 was, then, applied to measure the profiles of the actual and replicated cutting edges. The command displacement of Diamond Tool 2 actuated by the FTS was also set from 50 to 300 nm with an interval of 50 nm. However, the corresponding indentation depths were evaluated to be 35, 45, 77, 104, 127, and 163 nm according to the outputs of the inside and the outside sensors, which were different from those by the previous diamond tool with a nose radius of 1 mm.

The measured results of Diamond Tool 2 are summarized in Figure 13. The average radius of the diamond tool cutting edge was evaluated to be 41.29 nm with a standard deviation of 0.66 nm. The standard deviation of the evaluated uncertainty values was calculated to be 0.032 nm. The difference between the actual cutting edge radius by the proposed measurement method ($R_{\text{tool}}$) and the cutting edge radius imaged directly by the AFM ($R_{\text{tool,m}}$) of Diamond Tool 2 was evaluated to be 7.36 nm. This value was also close to the nominal AFM tip radius of 7 nm. The reliability of the proposed method was, thus, verified from the measurement results of Diamond Tool 2.

![Figure 13. Experimental results of measuring Diamond Tool 2.](image)

4. Summary

In this paper, we presented high-precision cutting edge radius measurement of single point diamond tools using an atomic force microscope and a reverse cutting edge artifact based on the edge reversal method. A reverse cutting-edge artifact with a high-precision depth was fabricated on a workpiece surface using the optimized operation of a newly designed nanoindentation system. Cutting edge radius was evaluated from two AFM images, including an AFM image of the actual cutting edge and an AFM image of the reverse cutting edge, from which the convolution effect of the AFM tip radius was reduced. Cutting edge radii of two diamond tools were evaluated. The first tool had a nose radius of 1 mm and the second tool had a nose radius of 2 mm. The difference between cutting edge radii evaluated by the proposed measurement method and that directly obtained from the AFM image was 9.64 nm for the first tool and 7.36 nm for the second tool. Both values were close to the AFM probe tip nominal radius of 7 nm, from which the feasibility and the reliability of the proposed method were demonstrated. The effect of the elastic recovery was investigated by scanning a group of reverse cutting edge artifacts with various depths from 20 to 180 nm. We confirmed that the elastic recovery of the reverse cutting edge did not affect the measurement accuracy of cutting edge radius when the indentation depth was within 20 to 200 nm. Three-dimensional profile measurements
of diamond tool cutting edge based on the proposed measurement method will be carried out in the future work.

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