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Three-dimensional simulations of gravitationally confined detonations compared to observations of SN 1991T

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ABSTRACT

The gravitationally confined detonation (GCD) model has been proposed as a possible explosion mechanism for Type Ia supernovae in the single-degenerate evolution channel. It starts with ignition of a deflagration in a single off-centre bubble in a near-Chandrasekhar-mass white dwarf. Driven by buoyancy, the deflagration flame rises in a narrow cone towards the surface. For the most part, the main component of the flow of the expanding ashes remains radial, but upon reaching the outer, low-pressure layers of the white dwarf, an additional lateral component develops. This causes the deflagration ashes to converge again at the opposite side, where the compression heats fuel and a detonation may be launched. We first performed five three-dimensional hydrodynamic simulations of the deflagration phase in 1.4 M⊙ carbon/oxygen white dwarfs at intermediate-resolution (2563 computational zones). We confirm that the closer the initial deflagration is ignited to the centre, the slower the buoyant rise and the longer the deflagration ashes takes to break out and close in on the opposite pole to collide. To test the GCD explosion model, we then performed a high-resolution (5123 computational zones) simulation for a model with an ignition spot offset near the upper limit of what is still justifiable, 200 km. This high-resolution simulation met our deliberately optimistic detonation criteria, and we initiated a detonation. The detonation burned through the white dwarf and led to its complete disruption. For this model, we determined detailed nucleosynthetic yields by post-processing 106 tracer particles with a 384 nuclide reaction network, and we present multi-band light curves and time-dependent optical spectra. We find that our synthetic observables show a prominent viewing-angle sensitivity in ultraviolet and blue wavelength bands, which contradicts observed SNe Ia. The strong dependence on the viewing angle is caused by the asymmetric distribution of the deflagration ashes in the outer ejecta layers. Finally, we compared our model to SN 1991T. The overall flux level of the model is slightly too low, and the model predicts pre-maximum light spectral features due to Ca, S, and Si that are too strong. Furthermore, the model chemical abundance stratification qualitatively disagrees with recent abundance tomography results in two key areas: our model lacks low-velocity stable Fe and instead has copious amounts of high-velocity 56Ni and stable Fe. We therefore do not find good agreement of the model with SN 1991T.

Key words: hydrodynamics – radiative transfer – methods: numerical – nuclear reactions, nucleosynthesis, abundances – supernovae: general – supernovae: individual: SN 1991T

1. Introduction

It is widely accepted that Type Ia supernovae (SNe Ia) are thermonuclear explosions of white dwarf stars. Since isolated white dwarfs are stable objects, the progenitor star must be interacting with a companion such that critical conditions necessary for explosion can be achieved. These critical conditions vary depending on the explosion mechanism, of which several have been proposed.

The manner in which the exploding, probably carbon-oxygen (CO), white dwarf (WD) accretes matter in the first place and the nature of the companion have been topics of debate for decades (Whelan & Iben 1973; Nomoto 1982; Iben & Tutukov 1984; Webbink 1984; Yungelson et al. 1995; Tutukov & Yungelson 1996; Yungelson & Livio 2000; Han & Podsiadlowski 2004; Ruiter et al. 2009, 2013; Mennekens et al. 2010; Toonen et al. 2012; Hillebrandt et al. 2013).

Different progenitor evolution scenarios exist, and for some scenarios yet again different explosion models have been proposed. For the single-degenerate scenario, for example, for pure deflagrations, deflagration-to-detonation transitions, pulsational reverse detonations, and gravitationally confined detonation (GCD) models have been suggested. Here we focus on the GCD model, first discussed by Plewa et al. (2004).
The GCD model starts with the ignition of a deflagration in a single off-centre bubble in a near-Chandrasekhar-mass (near-$M_{\text{Ch}}$) white dwarf (WD). Driven by buoyancy, the burning products of the deflagration quickly rise towards the stellar surface, where, in addition to the dominant radial expansion, they develop a lateral velocity component and converge at the opposite site. There, the flow compresses and heats still unburned fuel, and a detonation may be launched. To successfully trigger the detonation, flow convergence in rather dense material is required. Therefore, a weak deflagration and only a modest expansion of the WD is expected to favour the scenario (see Sect. 2.2). Consequently, the ensuing detonation burns a large amount of fuel at high densities, mostly $^{56}$Ni, thus producing bright SNe. Supernova 1991T (Filippenko et al. 1992; Phillips et al. 1992; Schmidt et al. 1994; Lira et al. 1998) is the prototypical event of a spectroscopically peculiar class of energetic and luminous SNe Ia. SN 1991T is the best characterised exemplar of a sub-class (SNe 91T) of SNe Ia that make up a few percent of all observed SNe Ia (Li et al. 2011; Silverman et al. 2012; Blondin et al. 2012). In contrast to normal SNe Ia, SNe 91T are known to occur preferentially in late-type galaxies (Hamuy et al. 2000; Howell 2001), indicating an origin in young stellar populations. SNe 91T further clearly distinguish themselves from normal SNe Ia by their peculiar pre-maximum light spectra. In particular, the characteristic Si $\lambda\lambda$5972, 6355 features prominent in normal SNe Ia (e.g. Branch et al. 1993) are essentially absent before maximum light; the same holds for other features of intermediate-mass elements, such as Ca $\Pi$ or S $\Pi$. Instead, early spectra show unusual Fe $\Pi$ features (Filippenko et al. 1992; Ruiz-Lapuente et al. 1992; Jeffery et al. 1992), requiring high ionisation and Fe abundance at high velocity. Moreover, SNe 91T events are more luminous by about 0.2–0.3 mag than the width-luminosity relation predicts for normal SNe Ia (Blondin et al. 2012).

At first sight, it is tempting to liken the GCD models with SNe 91T (e.g. Fisher & Jumper 2015). The deflagration ashes present at high velocities in the outer layers of GCD models result in a chemically mixed composition that is highly enriched with Fe-group isotopes at high velocities, which could explain key results obtained from interpreting observations of SN 1991T (e.g. Mazzali et al. 1995; Fisher et al. 1999; but see Sasdelli et al. 2014). Furthermore, the fact that only a few per cent of SNe Ia are classified as 91T-like (Li et al. 2011; Silverman et al. 2012; Blondin et al. 2012) would be naturally explained by the relative scarcity of the single-degenerate scenario compared to the violent-merger or double-detonation scenarios (e.g. Ruiter et al. 2009, 2011, 2013; Fisher & Jumper 2015). The identification of GCD explosions with SNe 91T is challenged from observations of the supernova remnant SNR 0509-67.5 in the LMC. First, based on light echo spectra, Rest et al. (2008) demonstrated clearly that this SN was a 1991T-like explosion. Second, Schaefer & Pagnotta (2012) ruled out the existence of a companion star in this SNR to very deep limits and thereby argued for a double-degenerate progenitor, which would exclude the canonical single-degenerate formation channel as a path to the GCD model. We note that García-Senz et al. (2016) have recently questioned the viability of the mechanism altogether, arguing that the Coriolis force substantially breaks the symmetry and thereby disfavours the emergence of a detonation.

Historically, both delayed-detonations in near-$M_{\text{Ch}}$ WDs (Mazzali et al. 1995) and sub-Chandrasekhar-mass (sub-$M_{\text{Ch}}$) double detonations (DDs; e.g. Liu et al. 1997) have been suggested as possible explosion models for SN 1991T. However, detailed comparisons of SN 1991T and synthetic spectra and light curves of bright sub-$M_{\text{Ch}}$ DD models (Kromer et al. 2010; Woosley & Kasen 2011) and bright near-$M_{\text{Ch}}$ delayed-detonation models (Sim et al. 2013) found substantial disagreement between the model predictions and the observations. Similarly, pure detonations of one WDs (Marquardt et al. 2015), which can produce SNe Ia with $^{56}$Ni masses around 1 $M_{\odot}$, are inadequate models for SNe 91T (for example, the strong Si $\Pi$ and Ca $\Pi$ absorption features present in the models before maximum light are almost absent in SNe 91T).

Although successful explosions of near-$M_{\text{Ch}}$ WDs in the GCD-framework have been obtained in several hydrodynamical explosion simulations (Plewa 2007; Meakin et al. 2009; Jordan et al. 2012a), only Meakin et al. (2009) have presented detailed isotopic yields for their 2D models. Kasen & Plewa (2007) presented broadband optical and near-infrared light curves, spectral time series, and spectropolarisation for their Y12 model and were generally successful in reproducing the basic properties of observed SNe Ia.

In this work, we present (multi-band) light curves and time-dependent optical spectra for an explosion model representative of the class of GCD models, for which we employed a detailed treatment of the nucleosynthesis for the detonation as well as for the deflagration. In Sect. 2 we briefly discuss our series of intermediate-resolution, single-bubble, off-centre deflagration simulations and present the evolution of a high-resolution model that met our very optimistic detonation criteria. In Sect. 4 we present spectra and light curves for this model and compare them with observations. In Sect. 5 we summarise and conclude that these synthetic observables do not resemble any known subclass of SNe Ia.

2. Hydrodynamic explosion simulations

According to theory, a detonation may spontaneously be initiated if a sufficiently shallow induction-time gradient can be set up to facilitate the formation of a shock in the shock-wave amplification through coherent energy release (SW ACER) mechanism (see e.g. Seitenzahl et al. 2009b). In the GCD model, suitable induction-time gradients may be obtained in the collision region near the stagnation point of the surface flow, directly opposite to the point of breakout of the rising deflagration bubble (Seitenzahl et al. 2009a). Since the spatial scales relevant to the initiation of a detonation cannot be resolved in full-star multi-dimensional explosion simulations (see the discussion in Seitenzahl et al. 2009a), it is common practice (e.g. Jordan et al. 2008, 2012a; Guillochon et al. 2010; Pakmor et al. 2011, 2012b) to pick a certain critical density $\rho_{\text{crit}}$ and temperature $T_{\text{crit}}$ that a cell composed of nuclear fuel must exceed for a detonation to be initiated. However, these critical values are no more than informed guesses based on separate high-resolution one-dimensional detonation initiation calculations (e.g. Niemeyer & Hillebrandt 1997; Seitenzahl et al. 2009b).

2.1. Computational method

We performed three-dimensional full-star simulations with the hydrodynamic supernova explosion code LEAFS. The whole exploding WD and the deflagration flame are captured separately on two different nested co-moving grids (Röpke 2005; Röpke et al. 2006). Since the flame is very thin compared to the radius of a near-$M_{\text{Ch}}$ WD, the former is treated as a sharp discontinuity with the help of the level set technique (Osher & Sethian 1988; Reinecke et al. 1999). The effective burning speed of the
The deflagration flame is composed of a laminar and a turbulent contribution (Pocheau 1994). For the former we used tabulated values from Timmes & Woosley (1992), while the turbulent flame speed was determined from a subgrid-scale turbulence model of Schmidt et al. (2006a,b). The energy release behind the deflagration level set is determined as a function of fuel density by interpolation in a table that is consistent with the energy release of a detailed nuclear reaction network; for details see Appendix A of Fink et al. (2014). The detonation was also modelled with a (separate) level set. For the detonation speed and energy release we used the tables of Fink et al. (2010), which, just as the deflagration tables, take the effects of incomplete burning at low densities into account. The reactive Euler equations are numerically solved with a finite-volume method (Fryxell et al. 1989) based on the piecewise-parabolic method (PPM) of Colella & Woodward (1984). For the nucleosynthesis, we post-processed one million tracer particles with a nuclear reaction network using the technique described in Travaglio et al. (2004) and Seitenzahl et al. (2010). The simulation code is essentially the same as described in Seitenzahl et al. (2013b), a key difference is, however, that the deflagration-to-detonation transition module was de-activated and the initiation of detonations is handled in a different way.

Here, we initialised the detonation around the grid cell in which both critical values \( \rho_{\text{crit}} \) and \( T_{\text{crit}} \) were (simultaneously) reached or exceeded first. Furthermore, to avoid artificial numerical triggering of the detonation, we required that the deflagration level set was at least one grid cell away and that the grid cell was composed of at least 90 per cent of unburned \( ^{16}\text{O} \) and \( ^{12}\text{C} \).

Our initial stellar model was an isothermal near-\( M_{\text{CH}} \) WD with a central density of \( 2.9 \times 10^9 \text{g \ cm}^{-3} \) and a temperature of \( 5 \times 10^5 \text{K} \). For the hydrodynamical simulations, the stellar material was assumed to be composed of carbon and oxygen where we approximated the effect of the assumed solar metallicity of the zero-age main-sequence progenitor on the stellar structure by initializing the electron fraction to \( Y_e = 0.49886 \) (see e.g. Seitenzahl et al. 2011).

\[ \approx \]

### 2.2. Moderate-resolution test cases

We ignited the deflagration in a single spherical off-centre region with a bubble radius of \( 10^6 \text{cm} \) and carried out simulations of five models at a moderate resolution of 256\(^3\) grid cells. The models varied only in the distance \( d_b \) of the centre of the ignition kernel to the centre of the white dwarf, and we tried \( d_b = 12, 37, 64, 125, \text{ and } 200 \text{ km} \). All ignitions occurred at a density greater than \( 2.3 \times 10^3 \text{g cm}^{-3} \).

The closer the initial deflagration is ignited to the centre, the slower the buoyant rise and the longer the deflagration ashes take to break out and close in on the opposite pole to collide. Since the white dwarf in the meantime continues to expand, obtaining high temperatures in the collision region at densities higher than \( \rho_{\text{crit}} \) becomes less probable. We thus find, as in Röpke et al. (2007), that larger distances of the ignition kernel from the centre of the white dwarf lead to more suitable conditions for a detonation at the closing point of the deflagration ashes. The reason is that the deflagration evolves faster, burns less mass, and releases less energy, which consequently leads to less pronounced expansion of the WD, so that when the erupted deflagration ashes converge, sufficiently high temperatures are more readily obtained at densities where detonations can occur (Townsley et al. 2007; Röpke et al. 2007; Aspden et al. 2011); see Malone et al. (2014) for an explanation of how background turbulence of the convective flow moderates this trend for very small offsets.

### 2.3. High-resolution simulation of model GCD200

Our main motivation for this work is not to elucidate whether a detonation can be triggered in the GCD framework, but rather what the predicted observables of the model look like if a detonation is triggered. We therefore chose a large offset for the ignition of the deflagration, 200km, which is more favourable to attaining detonation conditions than smaller offsets are. While 200km is still commensurate with the analytical calculations of García-Senz & Woosley (1995) and Woosley et al. (2004), the numerical simulations of Kuhlen et al. (2006) and Nonaka et al. (2012) favour much smaller offset distances. It is therefore questionable whether an offset of 200km for the ignition point is attainable at all.

Previous 3D hydrodynamics simulations with the LEAFS code (see Table 4 of Röpke et al. 2007) failed to obtain the more conservative detonation conditions \( \rho_{\text{crit}} = 10^6 \text{g cm}^{-3} \) and \( T_{\text{crit}} = 1.9 \times 10^9 \text{K} \), even for offset distances of the initial deflagration bubble as large as 200 km. Since we focus here on the model implications if a detonation occurs, we chose lower, less restrictive values for this work: \( \rho_{\text{crit}} = 10^9 \text{g cm}^{-3} \) and \( T_{\text{crit}} = 1.0 \times 10^9 \text{K} \). We also required the fuel content of the cell to be greater than 90 per cent, that is, \( X_{\text{fuel}} > 0.9 \). We note that this choice of critical detonation conditions is very optimistic, pushing the boundaries of the parameter space where detonations are expected to form through the gradient mechanism (Seitenzahl et al. 2009b).

We simulated a single-bubble ignition model with a bubble radius of \( 10^6 \text{cm} \) and \( d_b = 200 \text{km} \), with an increased resolution of 512\(^3\) grid cells (hereafter referred to as GCD200). This high-resolution model evolves to meet our critical detonation conditions (outlined above) at \( t = 2.37s \), and we initialised a single detonation around the grid cell where the constraints are first satisfied. The detonation was initiated by adding a second level set at this instant with positive values in a sphere of a radius of three cells (330 km) and converting this material instantaneously to iron group elements.

In Fig. 1 we show a two-dimensional slice of the temperature for two instants of time (2.20s and 2.37s). Most material at densities above \( 10^6 \text{g cm}^{-3} \) is unburned and the WD core (densities above \( 10^7 \text{g cm}^{-3} \)) appears spherical and hardly distorted by the deflagration. In the second snapshot, which corresponds to the time when we initiated the detonation, a hotspot is forming in the focus region in unburned material where the ashes of the deflagration converge. The central density of the white dwarf at this time (2.37s) is \( 6.6 \times 10^{10} \text{g cm}^{-3} \). The density and temperature in the grid cell around which the detonation is initialised are \( \rho_{\text{fuel}} = 1.09 \times 10^9 \text{g cm}^{-3} \) and \( T_{\text{fuel}} = 1.02 \times 10^8 \text{K} \). These thermodynamical conditions only satisfy the critical detonation criteria for this work, but would not have satisfied the more restrictive critical conditions of Röpke et al. (2007). Although our model was far from the more canonical and arguably more realistic detonation criteria \( \rho_{\text{crit}} \approx 1.0 \times 10^{10} \text{g cm}^{-3} \) and \( T_{\text{crit}} \approx 2.0 \times 10^9 \text{K} \) (Seitenzahl et al. 2009b), we cannot conclude about the likelihood of the formation of a detonation in GCD models in general. Our particular model represents only one specific realisation, albeit with a choice of offset of the initial deflagration bubble that is already most favourable for a detonation. For different setups or ignition parameters, for example different choices for the central density or composition, the situation may be different.
The progression of the explosion after the onset of the detonation is visualised in Fig. 2. The initialisation of the detonation, which occurs at $t \approx 2.37\, s$, is shown in the upper left panel of Fig. 2, where the detonation region is encircled. The detonation front propagates towards the central region of the white dwarf, which is predominantly composed of unburned $^{16}\text{O}$ and $^{12}\text{C}$. Since the central density is still rather high, most of the stellar material overun by the detonation is burned to iron group elements (IGEs), in particular to $^{56}\text{Ni}$. After burning ceases, the detonation ashes are surrounded by the deflagration ashes for most lines of sight, except for a small opening angle of reduced contamination around the detonation initiation site; see Fig. 2f.

In Fig. 3 we show the temporal evolution of the total ($E_{\text{tot}}$), nuclear ($E_{\text{nuc}}$), kinetic ($E_{\text{kin}}$), internal ($E_{\text{int}}$), and gravitational energy ($E_{\text{grav}}$) as functions of time. Energy conservation demands $E_{\text{tot}} = E_{\text{kin}} + E_{\text{int}} + E_{\text{nuc}} + E_{\text{grav}}$. We note that the sub-grid scale energy, which is of the order of 10$^{47}$ to 10$^{48}$ erg in turbulent deflagrations, is neglected here (see Fig. 1 in Schmidt et al. 2006b). Figure 3a shows model GCD200, while Fig. 3b shows the energies for the corresponding pure deflagration model, where no detonation is initialised. For the GCD simulation, the nuclear energy release is sufficient to unbind the entire white dwarf ($E_{\text{grav}}$ asymptotically approaches zero in the late explosion phase). If no detonation occurs, we obtain a supernova explosion that fails to fully unbind the WD and leaves behind a compact remnant after the deflagration flame extinguishes (Jordan et al. 2012b; Fink et al. 2014). Events like this have been shown to reproduce the observable characteristics of SN 2002cx-like SNe (Kromer et al. 2013).

3. Nucleosynthesis

Our postprocessing calculations are based on the 384 isotopes nuclear reaction network YANN (Pakmor et al. 2012a) that is run on the thermodynamic trajectories recorded by the tracer particles. The network employs the reaction rates from the JINA database (Cyburt et al. 2010) as of January 27, 2014. As outlined in Kromer et al. (2013), we implemented the effects of solar metallicity of the progenitor by initializing the tracer particle composition to 50\%$^{16}\text{O}$, 48.29\%$^{12}\text{C}$, and the remaining 1.71\% of the mass to the solar composition from Asplund et al. (2009) for elements heavier than He, with the exception of solar C, N, O, which we converted into $^{22}\text{Ne}$ to account for the effects of core He-burning.

The masses of stable isotopes after decaying all radioactive nuclides are given in Table 1. Radioactive species 100s after ignition are listed in Table 2. Burning in both deflagration and detonation yields 0.742 $M_\odot$ of $^{56}\text{Ni}$ and 0.030 $M_\odot$ and 0.037 $M_\odot$ of the stable iron group isotopes $^{54}\text{Fe}$ and $^{58}\text{Ni}$, respectively. The former is in large parts synthesised in the detonation phase, while the latter two also formed copiously in the deflagration near the centre where high densities favour neutronisation by electron capture reactions. However, the stable iron group isotopes synthesised in the deflagration do not remain at low velocity. They are carried towards the surface of the WD in the rising deflagration plumes and end up at the highest velocities, see Figs. 4 and 5.

Noteworthy, the GCD200 model has a sub-solar Mn-to-Fe production ratio of [Mn/Fe] = −0.13. This sub-solar ratio is a reflection of the fact that when the detonation is initiated, the central density of the WD has already fallen below the separation density between normal and $\alpha$-rich freeze-out, $\rho < 2 \times 10^8 \text{g cm}^{-3}$ (Thielemann et al. 1986; Bravo & Martínez-Pinedo 2012), where proton captures during the $\alpha$-rich freeze-out cause a lower Mn-to-Fe production ratio (e.g. Jordan et al. 2003; Seitenzahl et al. 2013a). Regardless of occurrence rate and although it originates from exploding near-$M_\odot$ WDs, our GCD model of near-$M_\odot$ SN 1a explosions therefore cannot explain the solar Mn-to-Fe ratio (see Seitenzahl et al. 2013a).

Using a smoothed-particle-hydrodynamics-like algorithm that approximately conserves the integrated yields (for details, see Kromer et al. 2010), we mapped the abundance and density structure of the SN ejecta at the end ($t = 100$ s) of the hydrodynamic simulations (by which point homologous expansion is a good approximation, e.g., Röpke 2005) to a 200$^3$ Cartesian grid. The resulting ejecta structure is shown in Fig. 4. We note the asymmetry of the model, with the ejecta in the upper hemisphere extending to much higher velocities. This asymmetric extent of the ejecta in velocity space is a natural consequence of the single spot near-surface lit detonation (Chamulak et al. 2012).
Fig. 2. Evolution of the GCD200 model for six different instances of time. The deflagration level set is shown in red and the detonation level set in blue. Since the deflagration ashes almost completely surround the detonation, we have rendered the deflagration level set semi-transparent to allow visualizing the enclosed detonation front. The spatial scales in the plots are $1.23 \times 10^{10}$ cm, $1.25 \times 10^{10}$ cm, $1.33 \times 10^{10}$ cm, $1.47 \times 10^{10}$ cm, $2.46 \times 10^{10}$ cm, and $1.59 \times 10^{12}$ cm for panels (a) to (f), respectively.

Fig. 3. Temporal evolution of $E_{\text{tot}}$, $E_{\text{nuc}}$, $E_{\text{kin}}$, $E_{\text{int}}$, and $E_{\text{grav}}$. The left panel shows model GCD200. The vertical line marks the time at which the detonation is initialised. The right panel is for the corresponding pure deflagration case when no detonation is initiated.

The direction of travel of the detonation points into the star on one hemisphere (with a component against the direction of expansion; along gravity) and points out of the star on the other hemisphere (with a component along the direction of expansion; against gravity), which leads to the systematic asymmetry of the ejecta.

The total mass of $^{56}$Ni produced is $0.74M_\odot$, hence we obtain a bright explosion. This $^{56}$Ni mass is very close to the $0.78M_\odot$ of $^{56}$Ni determined for SN 1991T by Sasdelli et al. (2014). Using the method of abundance tomography (Stehle et al. 2005), Sasdelli et al. (2014) also found that they required three per cent of $^{56}$Ni by mass at velocities above $12500$ km s$^{-1}$.
Table 1. Stable isotopes (asymptotic values) of model GCD200 in solar masses.

| Isotope | Mass $[M_{\odot}]$ | Isotope | Mass $[M_{\odot}]$ |
|---------|-------------------|---------|-------------------|
| $^1$H   | 6.19E−14          | $^2$H   | 0.00E+00          |
| $^3$He  | 0.00E+00          | $^4$He  | 1.29E−03          |
| $^6$Li  | 5.55E−21          | $^7$Li  | 1.61E−19          |
| $^9$Be  | 0.00E+00          | $^{10}$B | 7.92E−16          |
| $^{11}$B | 4.40E−12          | $^{12}$C | 1.88E−02          |
| $^{13}$C | 6.62E−08          | $^{14}$N | 1.49E−05          |
| $^{15}$N | 2.04E−08          | $^{16}$O | 1.13E−01          |
| $^{17}$O | 1.98E−06          | $^{18}$O | 2.54E−08          |
| $^{19}$F | 2.45E−10          | $^{20}$Ne | 6.83E−03          |
| $^{21}$Ne | 1.64E−06          | $^{22}$Ne | 6.73E−04          |
| $^{23}$Na | 1.16E−04          | $^{24}$Mg | 1.96E−02          |
| $^{25}$Mg | 1.68E−04          | $^{26}$Mg | 2.46E−04          |
| $^{27}$Al | 1.00E−03          | $^{28}$Si | 2.52E−01          |
| $^{29}$Si | 1.08E−03          | $^{30}$Si | 2.71E−03          |
| $^{31}$P | 5.39E−04          | $^{32}$S | 1.02E−01          |
| $^{33}$S | 2.36E−04          | $^{34}$S | 2.82E−03          |
| $^{36}$S | 2.63E−07          | $^{35}$Cl | 1.29E−04          |
| $^{37}$Cl | 2.15E−05          | $^{36}$Ar | 1.69E−02          |
| $^{38}$Ar | 1.21E−03          | $^{40}$Ar | 8.37E−09          |
| $^{39}$K | 6.58E−05          | $^{41}$K | 3.58E−06          |
| $^{40}$Ca | 1.49E−02          | $^{42}$Ca | 2.45E−05          |
| $^{43}$Ca | 2.91E−08          | $^{44}$Ca | 9.28E−06          |
| $^{46}$Ca | 2.58E−11          | $^{48}$Ca | 9.40E−16          |
| $^{45}$Sc | 1.34E−07          | $^{46}$Ti | 1.32E−05          |
| $^{47}$Ti | 4.58E−07          | $^{48}$Ti | 3.09E−04          |
| $^{49}$Ti | 2.31E−05          | $^{50}$Ti | 1.91E−10          |
| $^{50}$V | 1.30E−09          | $^{51}$V | 7.91E−05          |
| $^{50}$Cr | 3.31E−04          | $^{52}$Cr | 7.29E−03          |
| $^{53}$Cr | 7.40E−04          | $^{54}$Cr | 1.25E−07          |
| $^{55}$Mn | 4.91E−03          | $^{54}$Fe | 2.96E−02          |
| $^{56}$Fe | 7.43E−01          | $^{56}$Fe | 1.84E−02          |
| $^{58}$Fe | 7.04E−08          | $^{59}$Co | 3.45E−04          |
| $^{59}$Ni | 3.74E−02          | $^{60}$Ni | 1.50E−03          |
| $^{61}$Ni | 6.47E−05          | $^{62}$Ni | 5.24E−04          |
| $^{60}$Ni | 1.10E−13          | $^{63}$Cu | 3.08E−07          |
| $^{62}$Cu | 5.85E−08          | $^{64}$Zn | 9.31E−07          |
| $^{64}$Zn | 1.44E−06          | $^{67}$Zn | 7.72E−10          |
| $^{68}$Zn | 4.70E−10          | $^{70}$Zn | 4.81E−24          |
| $^{69}$Ga | 4.98E−15          | $^{71}$Ga | 7.24E−16          |
| $^{70}$Ge | 1.50E−15          | $^{72}$Ge | 4.70E−10          |

Table 2. Radioactive isotopes of model GCD200 at $t = 100$s in solar masses.

| Isotope | Mass $[M_{\odot}]$ | Isotope | Mass $[M_{\odot}]$ |
|---------|-------------------|---------|-------------------|
| $^{14}$C | 1.14E−05          | $^{22}$Na | 9.39E−09          |
| $^{26}$Al | 1.29E−06          | $^{32}$Si | 2.18E−08          |
| $^{32}$P | 5.36E−07          | $^{33}$P | 3.98E−07          |
| $^{35}$S | 5.25E−07          | $^{36}$Cl | 6.50E−07          |
| $^{37}$Ar | 2.08E−05          | $^{39}$Ar | 7.73E−09          |
| $^{40}$K | 3.86E−08          | $^{41}$Ca | 3.57E−06          |
| $^{44}$Ti | 9.26E−06          | $^{46}$V | 5.55E−08          |
| $^{49}$V | 2.14E−07          | $^{48}$Cr | 3.09E−04          |
| $^{49}$Cr | 2.29E−05          | $^{51}$Cr | 3.65E−06          |
| $^{51}$Mn | 7.55E−05          | $^{52}$Mn | 3.42E−06          |
| $^{53}$Mn | 4.82E−05          | $^{54}$Mn | 1.25E−07          |
| $^{56}$Fe | 7.23E−03          | $^{53}$Fe | 6.92E−04          |
| $^{55}$Fe | 1.35E−04          | $^{59}$Fe | 1.91E−15          |
| $^{60}$Fe | 7.93E−18          | $^{58}$Co | 4.77E−03          |
| $^{56}$Co | 2.40E−05          | $^{57}$Co | 2.77E−05          |
| $^{58}$Co | 6.64E−08          | $^{59}$Co | 9.99E−13          |
| $^{56}$Ni | 7.42E−01          | $^{57}$Ni | 1.84E−02          |
| $^{59}$Ni | 6.93E−05          | $^{58}$Ni | 7.11E−14          |
| $^{62}$Zn | 5.24E−04          | $^{62}$Zn | 3.53E−10          |
| $^{65}$Ga | 3.97E−08          | $^{68}$Ge | 4.70E−10          |

The high-velocity IGEs pose a problem to our model (when compared to SN 1991T): the shell of deflagration ashes has an IGE content of ~40 per cent by mass in almost every direction, which strongly contradicts Sasdelli et al. (2014). Furthermore, again in contrast to the result of Sasdelli et al. (2014), the GCD model does not predict a low-density core dominated by stable Fe. As expected, neutron-rich stable Fe-isotopes are produced at the highest densities where electron captures lower the electron fraction. For the GCD model, however, these products of the high-density burning unavoidably rise towards the surface due to buoyancy, even for the case of central ignition (Malone et al. 2014). A consequence of the buoyancy of the hot deflagration ashes is that the stable IGEs end up predominantly at the highest velocities (see Fig. 4 and top panel of Fig. 5). In contrast, the low-density core is dominated by $^{56}$Ni, which is synthesized in the detonation after the WD has expanded to lower central density. The high-velocity deflagration ashes are therefore a characteristic feature of the underlying explosion mechanism of the model, which indeed relies on the convergent flow of the deflagration products on the surface of the WD to trigger the detonation. The distribution of the intermediate mass elements, on the other hand, generally agrees quite well for a few prominent species such as O, S, and Si.

There is, however, more intriguing agreement between the special line of sight along the negative z-axis (bottom panel of Fig. 5) and several features of the abundance tomography results from Sasdelli et al. (2014). Since the deflagration ashes failed to fully surround the region where the detonation initiated, this particular line of sight is less contaminated by high-velocity deflagration ashes, which improves the comparison. Si and S for example peak between 10000 km s$^{-1}$ and 13000 km s$^{-1}$, O dominates the outer ejecta at high velocity (>12500 km s$^{-1}$), and $^{56}$Ni is present at high velocity at the few per cent level, all in good agreement with the tomography results of Sasdelli et al. (2014). The discrepancy concerning the absence of appreciable
I. R. Seitenzahl et al.: 3D GCD model vs. SN 1991T

Fig. 4. Final ejecta structure of model GCD200 in asymptotic velocity space at 100 s. We show the density (top left panel) and the mass fractions of select species in a slice through the midplane of the simulation volume along the x- and z-axes (detonation ignition occurred close to the negative z-axis).

low-velocity stable Fe however remains, and C is also much more abundant at high velocity in the model than in the tomography results. Still, this is the line of sight where the model resembles the observationally inferred abundance stratification the most. However, there is only a small solid angle of $\sim 0.38$ sr (corresponding to a cone of half-opening angle of $\lesssim 20^\circ$) where the deflagration ashes are nearly absent from the surface (see Fig. 4). This strongly argues against an identification of this special viewing direction with SNe 91T: a view of the supernova from a line of sight that intersects the deflagration ashes is more than thirty times more likely, and those viewing angles are lacking potential SN counterparts. In the next section, we present the results of our radiative transfer calculation for the GCD200 explosion model and compare the synthetic observables to SN 1991T.

4. Synthetic observables

To obtain synthetic spectra and light curves for the GCD200 model, we used the time-dependent 3D Monte Carlo radiative transfer code ARTIS (Kromer & Sim 2009; Sim 2007). For our radiative transfer simulation, we remapped the ejecta structure to a $50^3$ grid and followed the propagation of $10^8$ photon packets for 111 logarithmically spaced time-steps between 2 and 120 d after explosion. To reduce the computational costs, a grey approximation, as discussed by Kromer & Sim (2009), was used in optically thick cells, and for $t < 3$ d local thermodynamic equilibrium was assumed. We used the atomic data set described in Gall et al. (2012). Synthetic spectra for 121 equally sized viewing-angle bins covering the full solid angle were extracted on a 1000-bin logarithmic wavelength grid spanning a range between 600 and 30 000 Å.

On large scales, the GCD200 model is roughly symmetric under rotation about the axis defined by the centre of the star and the location of the initial deflagration bubble (the z-axis in Fig. 4). Thus, we can integrate the synthetic spectra over the equatorial angle with respect to the z-axis, leaving 11 equally sized viewing-angle bins in $\cos \theta$. Figure 6 shows snapshots of the spectral evolution of our model from 7.4 d to 33.6 d past explosion.

At early times ($t \lesssim 25$ d), the model spectra show a prominent viewing-angle sensitivity in the ultraviolet (UV) and blue wavelength regions where the flux level decreases from $\cos \theta = 1$ to $\cos \theta = -1$ by up to a factor 10 at certain wavelengths. This is due to the asymmetric distribution of the IGE-rich deflagration ashes: on the deflagration ignition side ($\cos \theta = 1$) IGEs are abundant up to $\sim 30000$ km s$^{-1}$, while the ejecta extend only to $\sim 20000$ km s$^{-1}$ on the far side ($\cos \theta = -1$) where the detonation ignites (see Fig. 4). This leads to a significant reduction of IGE line blanketing from $\cos \theta = 1$ to $\cos \theta = -1$ and thus an enhancement of the flux in the UV and blue regions when viewed from the detonation side. Redder wavelengths ($\lambda \gtrsim 5000$ Å) are not affected by line blanketing from IGEs and thus show no prominent viewing-angle sensitivity. At later times ($t \gtrsim 25$ d), the outer layers become optically thin and the viewing-angle sensitivity in the blue bands decreases. The remaining viewing-angle
Fig. 5. Final ejecta structure of model GCD200 along the positive (top) and negative (bottom) z-axis in asymptotic velocity space at 100 s. Detonation ignition occurred close to the negative z-axis. The relative absence of high-velocity IGE in this direction is a reflection of the lack of deflagration ashes (see Fig. 4). The profiles along the ±x-axis and ±y-axis qualitatively resemble the top panel.

sensitivity is mainly due to the off-centre structure of the detonation ashes (see Fig. 4).

The same behaviour can also be observed in the synthetic light curves (Fig. 7), which show a strong variation around the peak in the U and B bands. For U, the peak magnitudes vary between \(-18.9\) and \(-20.1\) mag with rise times between \(16.8\) and \(17.5\) d. The B-band light curves peak between \(19.2\) and \(19.9\) d at magnitudes between \(-19.3\) and \(-19.8\) mag. In contrast, we do not observe any significant variation in V, R, and I. After maximum the viewing angle sensitivity also decreases in the bluer bands.

The U- and B-band light curves show an additional effect at very early epochs (\(t \lesssim 5\) d). At these epochs γ-rays from \(^{56}\)Ni decay in the deflagration ashes are still trapped, leading to additional surface heating and an enhanced flux in the UV. This causes a decline in the U-band light curves at the earliest epochs and a plateau-like behaviour in the B band.

Figure 7 also shows light curves for three observed SNe Ia: the luminous SN 1991T (Lira et al. 1998) as well as SN 2004eo (Pastorello et al. 2007a) and SN 2005cf (Pastorello et al. 2007b), which are representative for the class of normal SNe Ia. Our model light curves are not a particularly good fit to any of these objects. Compared to normal SN Ia, the model light curves are clearly too bright. This is expected because the \(^{56}\)Ni mass of our model (\(0.74 M_\odot\)) is significantly higher than the typical range of \(0.4\) to \(0.6 M_\odot\) inferred for most SNe Ia (Scalzo et al. 2014). Compared to SN 1991T, an equatorial viewing angle (\(\cos \theta = 0\)) is in reasonable agreement with the observed B- and V-band light curves for \(t \lesssim 10\) d and \(t \gtrsim 30\) d. However, around the peak a viewing angle close to the deflagration ignition side agrees better with the observed B-band light curve of SN 1991T, while in the V-band our model is significantly too bright for all viewing angles.

Our model spectra also fail to convincingly match observed SN Ia spectra. Compared to normal SN Ia, the line features associated with intermediate-mass elements (IMEs) are slightly too weak. Si II \(\lambda 5972\), for example, is very weak in the model spectra, indicating relatively high ionisation and temperature of the ejecta. This is corroborated by the presence of absorption features at \(\sim 4200\) and \(4900\) Å that are attributed to Fe III. Compared
Fig. 6. Time sequence of synthetic spectra for our model (lines of different colours correspond to different viewing angles as indicated by the colour bar). The snapshot at 19.3 d corresponds roughly to $B$-band maximum in the model, which occurs between 19.2 and 19.9 d depending on the viewing angle. The synthetic spectra have been smoothed with a Savitzky-Golay filter to reduce Monte Carlo noise. For comparison we overplot observed spectra of SN 1991T at corresponding epochs (black, the flux calibration has been checked against the photometry and adjusted when necessary). The observed spectra have been de-reddened ($E(B-V) = 0.13$, Phillips et al. 1992) and de-redshifted ($z = 0.006059$, from interstellar Na). We assumed a distance modulus of 30.76 to SN 1991T (Saha et al. 2006).

Fig. 7. Synthetic broadband light curves for our model. Lines of different colour correspond to different viewing angles as indicated by the colour bar. Overplotted are observed light curves for the normal SNe Ia 2004eo (grey circles) and 2005cf (grey squares), and for the overluminous SN 1991T (black triangles). For the comparison we assume a $B$-band rise time of 19.6 d, which corresponds to the average $B$-band rise time of our model.

to SN 1991T, there is no individual viewing angle that provides good agreement over the full wavelength range and multiple epochs (see Fig. 6). Although relatively weak, the IME features of our model are still too strong at pre-maximum epochs when SN 1991T shows no clear signs of the Ca II H&K lines and Si II $\lambda 5624$. Si II $\lambda 6355$ develops in SN 1991T a week before maximum, but it is also weaker than in our model.

5. Summary and conclusions

The purpose of this work is to calculate the generic observables of a GCD model if a detonation occurs, not to settle the question whether a detonation can form in the first place. Deflagrations that are ignited closer to the centre lead to more burning and expansion, which leads to a weaker collision of the deflagration ashes at the opposite point of break-out. To obtain detonation conditions and a subsequent GCD SN explosion, we ignited a near-$M_{\text{Ch}}$ WD outside the preferred range predicted by numerical simulations (Nonaka et al. 2012) and chose less stringent critical detonation conditions compared to previous works (cf. Röpke et al. 2007).
Our high-resolution model (512^3) was ignited (200 km) and fulfilled our deliberately optimistic critical detonation conditions, and we initialised a detonation and followed the explosion until homologous expansion. Given the large offset, relatively little mass burned in the deflagration, which resulted in a relatively compact WD at the instant of detonation initiation. This means that GCD explosions are automatically linked to the brighter end of the SN Ia distribution. If the WD were ignited closer to the centre, we would obtain a stronger deflagration, resulting in stronger explosion, no detonation, and a sub-luminous SN 2002cx-like event (Jordan et al. 2012b; Kromer et al. 2013).

By post-processing one million tracer particles with a nuclear reaction network, we determined the detailed nucleosynthesis in the explosion. A high-velocity outer shell of deflagration ashes rich in ^{56}Ni and stable iron group isotopes such as ^{54}Fe and ^{58}Ni is a generic and robust prediction for this class of models. This shell of IGE-rich deflagration ashes exhibits a gradient in its extent in velocity space, decreasing in extent from the deflagration-ignition side to the far side where the detonation-initiation is located.

We used the resulting three-dimensional composition structure of the explosion ejecta as input for a Monte Carlo radiative transfer calculation with the ARTIS code to obtain time-dependent spectra and light curves for the GCD200 model. Comparing these synthetic observables to SN Ia data, we conclude that this GCD model cannot explain any of the more common sub-classes of SNe Ia. In particular, it fails to explain SN 1991T-like events, a class of SNe that owing to their brightness and early high-velocity Fe-features appeared to be the most natural candidate (Fisher & Juniper 2015). First, the single-spot ignition of the deflagration on one side of the star and the initiation of the detonation on the opposite side naturally leads to an asymmetric extent of the shell of deflagration ashes in velocity space, extending to much higher velocity on the side where the deflagration was ignited. This in turn leads to a strong viewing-angle dependence for the synthetic spectra and light curves, most pronounced in the bluer bands at early times, which disagrees with observations. Since the ejecta asymmetry is a generic feature of GCD explosions (Chamulak et al. 2012), the resulting viewing angle sensitivity is generic as well. Identification of SNe 91T with only the peculiar line of sight towards the location of the initiation of the detonation, which gives the best agreement, leads to the following problem: the other viewing angles characterised by high-velocity turbulently mixed deflagration ashes rich in ^{56}Ni and stable IGE statistically dominate and do not correspond to a known more common sub-class of SNe. Second, our model is too abundant in IGEs at high velocity and lacks the stable low-velocity Fe inferred by Sasdelli et al. (2014) by abundance tomography methods. Third, although the overall flux-levels compare favourably, the spectral features do not. For example the Ca II H&K lines, Si II A6564, and Si II A6555, which are absent or very weak pre-maximum in SN 1991T, are too strong in our model for all lines of sight. Particularly the first two points are very reliable generic features of GCD explosion models. Overall, our results therefore suggest that GCD is probably not a good explosion model for SN 1991T. Whether more peculiar events can be explained by GCD events remains to be seen.

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A57, page 10 of 11
