On the use of satellite-derived frontal metrics in time series analyses of shelf-sea fronts, a study of the Celtic Sea

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LS and RW developed the concept. Monthly level-4 composites of the various frontal metrics used in the analysis were provided by PM as 8bit raster files. Data processing and analysis was carried out by LS. Manuscript was written by LS and revised by all authors.

Abstract
Satellite-derived frontal metrics describe characteristics of oceanic thermal fronts, such as their strength or persistence. They are used in marine science to investigate spatio-temporal variability of thermal fronts or in ecological studies to assist in explaining animal distributions. Although these metrics represent highly processed data, which is based on sometimes complex algorithms, little guidance is available on their correct application in quantitative analyses, in particular for non-specialist users. This research aims to improve accurate use of frontal data. This case study investigates the inter-annual and seasonal variability of two tidal mixing fronts on the Celtic Sea shelf, based on monthly time series of daily frontal maps at ~1km² resolution from 1990 to 2010. Some metrics are almost identical and can be grouped, e.g. frontal probability, persistence and so-called "composites" (Pearson correlation: r=0.8-1.0; p<0.001), whereas the metric describing frontal strength is distinct from other ones. Consequently, strength and metrics of the frontal probability group showed pronounced differences in their inter-annual and seasonal variability: Strength displayed an oscillating pattern between 1990 and 2010 while there were no significant changes in probability over time. In addition, seasonal variability was affected by segments from adjacent fronts, not belonging to the fronts of interest, which could result in biased estimates.
Most important, there was a doubling of available satellite imagery between 1990 and 2010 due to a greater number of operational satellites, which negatively affected frontal probability, positively frontal strength and consequently, changed the temporal pattern of both. When using frontal maps for temporal analyses, we should choose the metric carefully, be aware of biased estimates caused by variability from unwanted frontal segments in the data and account for the variable data quantity. This guide on the use of frontal metrics will be helpful to improve correct interpretations of statistical analyses.

1 Introduction

Marine thermal fronts are transition zones in which steep gradients in temperature can be observed over a relatively small distance, often associated with changes in other physical properties, complex hydrodynamics and elevated biomass. Thermal fronts occur over a wide range of spatio-temporal scales, ranging from the large-scale Polar Front to small, short-lived tidal intrusion (Owen, 1981). Frontal metrics derived from remote sensing satellite imagery describe characteristics of these thermal fronts, such as their strength or frequency, in the area of interest and for a desired period. They come in the form of images called frontal maps, which are usually a fusion of multiple satellite images, because single images are often cloud-covered (Miller, 2009). Combining multiple images into one map creates (ideally) a cloud free view on the ocean surface. The resulting frontal maps are a mosaic of pixels containing values describing a front (frontal values) or not (cloud free pixel that cover an area of sea without fronts). The frontal maps provide information on the surface signal of thermal fronts over large spatio-temporal scales, which makes them very popular for scientists from a variety of backgrounds, including oceanographers and ecologists.

Frontal maps are particularly applicable to the study of large-scale processes because of their spatio-temporal coverage: a global and contiguous time series since the 1980’s. They have been used to describe their spatio-temporal variability (Hopkins et al. 2010; Lee et al., 2015; Park et al. 2007; Belkin et al., 2009; Nieblas et al. 2014; Oram et al. 2008) and to create maps of surface fronts all over the world (e.g. Canary Upwelling System: Nieto et al., 2012; the Pacific Ocean: Belkin and Cornillon, 2003; Canadian waters: Cry & Larouche, 2015; California Current System: Armstrong et al., 2012; Indian Ocean: Roa-Pascuali et al. 2015; Japanese Coast: Shimada et al. 2008). Satellite-derived frontal metrics have also become popular in recent years amongst marine ecologists to explain and predict species distributions, particularly for marine apex predators (e.g. Bauer et al. 2015; Nieto et. al 2017; Priede et al. 2009). The potential of fronts to act as biodiversity hotspots has also received attention from
policymakers involved in development of spatial conservation measures such as Marine Protected Areas (MPAs), and future monitoring of mobile species as part of the Marine Strategy Framework Directive (MSFD) (Defra, 2009; 2012; European Union, 2008). Initially, frontal maps were used only descriptively and compared to tracks or distribution maps of marine biota (Doniol-Valcroze et al., 2007; Edwards et al., 2013; McClathie et al. 2012; Wingfield et al. 2011). Now, they are increasingly used in statistical models to investigate bio-physical coupling and ecosystem dynamics (Broodie et al. 2015; Pirotta et al., 2014; Xu et al. 2017).

Frontal metrics represent highly processed data and can be based on complex algorithms, making it difficult for the user to understand the meaning and their limitations when applying statistical analyses, particular for scientist not specialised in the field of remote frontal detection. Although results of quantitative analyses can vary depending on the metric employed, not much guidance for researchers is available in the scientific literature on the use of frontal metrics, the differences between them and factors to consider during their statistical processing. Considering the complex process of generating frontal maps and metrics, this represents essential information for users outside the field to ensure best practice and avoid pitfalls during quantitative analysis.

There is also a lack of information regarding factors influencing the metrics directly, such as the quantity of data used to create a frontal map or the effect of spatial averaging over larger areas in order to create time series. However, it is essential to consider these factors in order to avoid incorrect estimates of a front. For example, there has been a steep and continuous increase in satellite passes over the past 20 years, resulting in an increased number of satellite images per day and therefore, higher data quantity, which affects temporal variability pattern (Oram et al. 2008). Although varying sampling size can affect the results of statistical analyses, not many studies concerning long-term trends of satellite-derived frontal metrics account for this (e.g. Belkin et al., 2005; Kahru et al., 2012; Ullman et al., 2007). Some studies ensure data quality during the processing stage, e.g. only images with at least 90% cloud-free pixels are used, but do not account for data quantity during statistical analysis (Obenour 2013).

This paper provides guidance on the use frontal metrics and their quantitative analysis, particularly directed towards users outside remote frontal detection. We demonstrate the necessity to account for influencing factors and how to deal with them, including i) a strong non-linear effect of data quantity, ii) bias introduced by not distinguishing between different frontal types and iii) the choice of metric to be used. We show how these factors influence the
distinct temporal pattern of some commonly used frontal metrics over 20 years from January 1990 to December 2010. The focus of this study are two tidal mixing fronts, which form in the Celtic Sea during the spring when the water is stratified, namely the Celtic Sea and Ushant Front. These two fronts separate the Celtic Sea from the Irish Sea and Western English Channel respectively (Figure 1). Tidal mixing fronts are transition zones between tidally-mixed coastal and seasonally-stratified shelf waters and are critical in shaping oceanographic and biological processes during the summer months (LeFevre, 1986; Simpson and Sharples, 2012). The temporal variability of the Celtic Sea and Ushant Front is well documented from four decades of in-situ and modelling studies (Brown et al., 2003; Elliott et al., 1991; Holt et al., 2010; Neil et al., 2013; Pingree et al., 1978; Young et al., 2004), which provide a reference for the results of this research.
Figure 1 (colour): Average frontal density map (June 2009) showing thermal fronts of the Celtic Sea. Red colours refer to higher frontal density and blue colours to no frontal density. The white dotted circles highlight the tidal mixing fronts UF=Ushant Front, SIF=Scilly Isles Front, CSF=Celtic Sea Front and the shelf break front=SBF. The white polygons refer to the two sampling areas used in this research (Celtic Sea and Ushant Front). Parametrisation of the boundary definition for the two front polygons can be found in section 2.4 and in the supplement.

2 Methods

2.1 Processing of frontal maps

Frontal maps used in this research are based on Advanced Very High Resolution Radiometer (AVHRR) data from National Oceanic and Atmospheric Administration (NOAA) satellites from January 1990 to December 2010. The frontal data were processed specifically for this study prior to statistical analysis, using a consistent methodology to produce a multi-decadal time-series for the purpose of exploring the applicability of different front metrics to such analyses. These raw data were acquired, translated into SST values, geo-corrected, cloud masked, and mapped at 1.1 km² resolution by the NERC Observation Data Acquisition and Analysis Service (NEODAAS) (www.neodaas.ac.uk/data). Both day and night images were considered in order to maximise the detection of fronts in frequently cloud-covered regions: diurnal variations in SST cause negligible effect on front maps because the fronts are detected and their gradients estimated on individual SST scenes rather than on composite maps. In addition, differences are likely to be small, because we are detecting and searching for a particular type of front exactly where it occurs. Fronts were detected on each satellite image by application of the Single Image Edge Detection algorithm (SIED) developed by Cayula and Cornillon (1992). In this approach, a histogram of the SST frequency distribution is created, based on a user-defined array of pixels, but usually 32x32 pixels (also used in this research). If the histogram has a bimodal form, it suggests the presence of two different water masses. In order to qualify as two separate water masses, the temperature difference between the two populations has to be at least 0.4°C as recommended when applied to low-noise SST data (Miller, 2009). The SIED then marks the transitional values between the two modes of the histogram as valid pixels = frontal (Fvalid).

A SIED-derived frontal map from a single satellite image is unsuitable for the description of meso-scale features due to their high spatio-temporal variability and the frequency of cloud cover in the study region, which disguises dynamic processes (Miller, 2009). Therefore, in this research we aggregated daily front detections into monthly composite maps for each
metric define below, in order to highlight stable frontal features (Miller, 2009). Although higher temporal resolution would have been more desirable to investigate seasonal pattern of tidal mixing fronts, weekly and fortnightly frontal maps were still highly affected by cloud cover (even during the summer months and particularly at the beginning of the study period in the early 1990’s) and were unsuitable for the analysis. In addition, the resolution of the frontal maps was scaled down to 4.8km² by taking the mean of a four by four pixel array on the final map. Spatial downscaling was performed to reduce variability around the frontal contours, which facilitated the determination of the sampling area (see supplementary section 6.1). Further steps of data processing depend on the metric chosen and are explained in detail in section 2.2.

2.1.1 Spatial averaging of frontal pixels over the sampling area
To investigate inter-annual and seasonal variability of the selected frontal metrics at the Celtic Sea and Ushant Front, a time series for each metric had to be created. For this, all pixels within each of the two frontal areas were spatially averaged to obtain a single value per front and monthly map. We considered all pixels, clear and valid ones in order to avoid bias introduced by variable sample size, e.g. there are more frontal pixels during the summer. The position of tidal mixing fronts varies seasonally, in response to tidal movements, storm events and other factors. Therefore, the sampling area for each front needed to be large enough to capture the spatial variability of the fronts, but small enough to exclude unwanted features in the vicinity as much as possible, which could bias estimates of the fronts of interest (e.g. other fronts such as river plumes or coastal currents). In order to identify a suitable sampling area, core frontal areas were visually identified using $F_{comp}$ maps for the Celtic Sea and Ushant Front. Position and extend of each front are known from previous studies (Eliot and Clarke, 1991; Horsburgh et al., 1998; Pingree, 1975; Simpson et al., 1981; Young et al., 2004). Based around the core area, different sized subsets were created, which were resampled to find the most suitable sampling area and to ensure no bias caused by an area size effect was introduced. Details of the resampling approach can be found in the supplement (Section 6.1)

2.2 Frontal metrics used in this research
In the following description, the word image refers to a satellite image of the study area, which consists of an array of pixels. Maps refer to the satellite images after frontal algorithms have been applied and show frontal metrics. The example pixel is at a given location of an image (e.g. uppermost left corner), on a map or over a sequence.
**Fclear and Fvalid:** For each pixel in the monthly map, Fclear and Fvalid simply provide the total amount of clear and valid pixels respectively. Valid pixels (Fvalid) are pixels that have been identified by the SIED-algorithm as frontal (described in section 2.1). Clear pixels are pixels that were not cloud covered and had a clear satellite view on the ocean, whether or not a front was observed. For example, if 40 images were obtained over the period of one month, 30 of these had clear views on an example pixel, and in the other ten images this pixel was obscured by clouds, the Fclear value for this pixel would be 30. Out of the 30 clear views, if the example pixel was identified as a front 20 times by the SIED-algorithm, the Fvalid would be 20.

**Fprob** (Figure 2 and Table 1) represents the probability of observing a front in a given pixel over the sequence of images used (Miller, 2009). As in the example above, out of the 30 clear views, if the example pixel was identified as a front 20 times by the SIED-algorithm, then the Fprob value for this pixel would be:

\[
F_{\text{prob}} = \frac{\text{front pixels}}{\text{clear pixels}} = \frac{20}{30} = 0.67.
\]

Frontal (also called valid) and clear pixels are described in more detail further below under Fvalid and Fclear. The higher the Fprob value, the more often a front was detected in the pixel. Therefore, clusters of pixels with high Fprob on a frontal map represent areas of higher frontal occurrences. The advantage of Fprob is that it is simple and easy to understand. However, there are two apparent disadvantages. Firstly, it is a proportion and can easily be biased when the relationship between the numerator and denominator is not linear or if both change in the same direction, but at different rates. Secondly, Fprob does not provide information on the strength of a front.

**Fmean** provides information on the temperature gradient (temperature change per distance of pixel resolution, in this case °C/4.8km²) and hence, an indication of the strength of a front (Miller, 2009). After applying the SIED-algorithm to a single image, the temperature gradients between a front pixel and its neighbouring pixels are calculated. The value of the greatest gradient found is assigned to the example pixel. This is done for all valid pixels on a map and all images going into a map. For the monthly map, the mean of all temperature gradient values is calculated for the example pixel. However, the mean is only based on front pixels in the sequence and not on pixels that were cloud free but non-frontal as it is the case for Fprob. This is in order to avoid degrading the metric with gradients not associated with fronts, or with low gradients observed where a dynamic front was previously located. Using
the same example as above, the temperature gradient was calculated for the 20 front
observations of the example pixel.:

\[
F_{mean} = \frac{\text{sum of gradient values (20 different values)}}{\text{total number of frontal pixels}} = \frac{21.4}{20} = 1.07
\]

It should be noted that \(F_{mean}\) disregards of clear pixels. One the one hand, this makes
\(F_{mean}\) less sensitive to data quantity (\(F_{clear}\)) and does lessen the visualisation of ephermal
features. On the other hand, it does not distinguish between pixels that were identified as
frontal frequently versus ones that were not. For instance, the example pixel was identified as
frontal 20 times in the sequence of 30 clear images and had an \(F_{mean}\) of 1.07. Another pixel
has been identified as frontal twice in the sequence of 30 clear images, but also had a
temperature gradient of 1.07 each time. This pixel will receive the same value on the map as
first one although its frontal frequency was very small. This results in maps containing many
transient frontal segments that are displayed with the same strength as the persistent ones,
which can introduce noise to a map.

\(F_{pers}\) is the product of multiplying the final (in our case monthly) map of \(F_{mean}\) by the final
map of \(F_{prob}\):

\[
F_{pers_{final}} = F_{mean_{final}} \times F_{prob_{final}}
\]

By weighting \(F_{mean}\) by a measure of persistence (\(F_{prob}\)), areas of frequently occurring
fronts are highlighted and noise introduced by short-lived frontal segments is reduced (Miller,
2009). While the multiplication of \(F_{prob}\) and \(F_{mean}\) aids visualisation of more consistent
features, it complicates interpretation of the metric itself, because it is comprised of two
entities that have different meanings. A change in \(F_{pers}\) cannot be directly attributed to
either changes in \(F_{prob}\) or \(F_{mean}\) (or both), whereas it might be crucial to know which
metric is more affected, e.g. if interested in the meteorological drivers of the observed
variability.

In \(F_{comp}\) maps an additional weighting factor is applied to the monthly map of \(F_{pers}\), which
considers the spatial proximity of frontal pixels (Miller, 2009):

\[
F_{comp_{final}} = F_{pers_{final}} \times \text{weighting factor}
\]
Pixels near or in clusters of valid pixels, will receive an additional boost. The closer the pixel is to a frontal cluster, the more it will be boosted. This process will ignore pixels located beyond a certain distance from any frontal clusters. The resulting maps further emphasise persistent features and further reduce the occurrence of noise. Like $F_{pers}$, $F_{comp}$ obscures the influence of each of the components for the final product and it is not possible to identify the most variable component.

$F_{dens}$ is an $F_{comp}$ map with an additional spatial smoother (in this case a Gaussian filter of five pixels width) applied to the final $F_{comp}$ map in order to turn the discrete front segments into a continuously-varying spatial map (Scales et al., 2015). $F_{dens}$ is particularly useful for visualisation of persistent, spatially stable features as it removes nearly all transient frontal segments:

$$F_{dens_{final}} = F_{comp_{final}} \times \text{spatial smoother}$$

| Metric | Common name | Definition | Value range |
|--------|-------------|------------|-------------|
| $F_{valid}$ | Valid pixels | Total of valid (frontal) pixels in a sequence of images | Any positive integer |
| $F_{clear}$ | Clear pixels | Total of clear pixels in a sequence of images | Any positive integer |
| $F_{prob}$ | Frontal probability | $F_{valid} \div F_{clear}$ | 0-1 |
| $F_{mean}$ | Temperature gradient | $\frac{\text{Temperature gradient}}{F_{valid}}$ | 0-2.54 |
| $F_{pers}$ | Frontal persistence | $F_{prob} \times F_{mean}$ | 0-0.254 |
| $F_{comp}$ | Frontal composite | $F_{pers} \times F_{prox}$ | 0-0.254 |
| $F_{dens}$ | Frontal density | $F_{comp} + \text{spatial smoother}$ | 0-0.254 |

Table 1: List of metrics used in this research and their abbreviations, common names, quantitative derivation and value range. All are at monthly 4.8km$^2$ resolution.
Figure 2 (colour): Monthly maps for $F_{\text{valid}}$, $F_{\text{prob}}$, $F_{\text{mean}}$, $F_{\text{pers}}$, $F_{\text{comp}}$ and $F_{\text{dens}}$ from June 2009. Pixels covering land are no-value pixels and therefore, come up as white.
2.3 Statistical analyses

Correlation analyses showed that the metrics $F_{prob}$, $F_{pers}$, $F_{comp}$ were strongly related. $F_{dens}$ displayed highest correlations with $F_{comp}$ and $F_{mean}$ (Table 2). Subsequently, analyses in this research were conducted on $F_{prob}$ (representative for the group $F_{prob}$, $F_{comp}$ and $F_{pers}$) and $F_{mean}$ only. $F_{prob}$ was selected because it is a) more comprehensible than other complex metrics, b) frequently used in remote sensing research, and c) the driving component in $F_{comp}$ and $F_{pers}$ in our dataset (although this can differ in other systems, e.g. California Current System, Nieto et al. 2012). $F_{mean}$ has been less frequently used in ecological or oceanographic time series, but is included because it provides useful information on the strength of the front and hence, other characteristics than $F_{prob}$.

Table 2: Pearson Product Moment correlation coefficients ($r$) after extraction of the seasonal variability for all metrics combinations. Lower left diagonal (blue font) refers to Celtic Sea Front and upper right diagonal (black font) to Ushant Front correlations. Coefficients above 0.7 are in bold and, italic numbers are coefficients of correlation analyses with p-values <0.05.

| Metric/ $r$ | $F_{prob}$ | $F_{pers}$ | $F_{comp}$ | $F_{mean}$ | $F_{dens}$ |
|------------|------------|------------|------------|------------|------------|
| $F_{prob}$ | -          | 0.9        | 0.9        | -0.04      | 0.3        |
| $F_{pers}$ | 0.9        | -          | 1.0        | 0.2        | 0.5        |
| $F_{comp}$ | 0.9        | 1.0        | -          | 0.2        | 0.6        |
| $F_{mean}$ | -0.3       | 0.06       | 0.06       | -          | 0.6        |
| $F_{dens}$ | 0.3        | 0.5        | 0.6        | 0.6        | -          |

Inter-annual and seasonal variability of $F_{prob}$ and $F_{mean}$ and the effect of $F_{clear}$ on this variability were investigated using anomalies. Anomalies for statistical analysis were created by subtracting the overall mean of the time series from each data point of the time series (each month-year combination). Temporal explanatory variables were year to account for interannual variability, month to account for seasonal variability and $F_{clear}$ to account for variations in data quantity. To demonstrate the effect of $F_{clear}$ on $F_{prob}$ and $F_{mean}$, predictions of monthly and yearly variability of the two metrics are shown from two models, one with and one without the $F_{clear}$ variable. For visualisation purposes, monthly and yearly anomalies were calculated by subtracting the overall mean from the mean of each month/year respectively. For inter-annual variability plots only months March to November were considered (see below) to avoid the unwanted inclusion of wintertime fronts (present in the study area) not associated with the tidal mixing fronts.

Generalized Additive Mixed Models (GAMMs) with an autoregressive correlation structure of order one (AR(1)) were used in order to account for temporal autocorrelation and the non-linear relationship between the response and explanatory variables. The GAMMs take the
structure as specified by Hastie and Tibshirani (1987) and were fitted using the `gamm` function in the `mgcv` package (Wood, 2006). Smoothed terms were fitted as regression splines with fixed maximum degrees of freedom (k=6) for the covariate `month` and `Fc` in order to avoid overfitting. The variable `month` was modelled using cyclic cubic regression splines, setting knots manually between 3 (March) and 11 (November) in order to account for the circular nature of this term. Model selection was conducted using manual stepwise-backwards selection. Model fit was examined by means of residual analysis. Residual analysis displayed a few single outliers in the Celtic `Fprob` model. The outliers were excluded and the model re-run, which improved model fit, but did not affect significances of the variables.

3 Results

3.1 Temporal variability of `Fprob` and `Fmean`

Due to the distinct nature of the two metrics, their temporal patterns differed significantly. `Fprob` anomalies were positive until 1996 and dropped sharply thereafter at both fronts. Apart from minor variations, temporal variability of `Fprob` was consistent for the remainder of the time series. Extremely high values of `Fprob` were observed in 1990 and 1996 at the Celtic Sea Front, which were less pronounced at the Ushant Front. In contrast to `Fprob`, `Fmean` displayed temporal fluctuations with an initial decrease from 1990 to 1996, followed by an increase from 1997 to 2010 at both fronts (Figure 3). A notable low in `Fmean` occurred in 1996 at the Celtic Sea and Ushant Front. Overall differences between the Celtic Sea and Ushant Front were low for each metric and occurred predominantly in the first ten years of the time series. In addition, values for both metrics were slightly higher at the Celtic Front compared to the Ushant Front: `Fprob` Celtic: 0.078±0.03, Ushant: 0.072±0.03; `Fmean` Celtic: 0.22±0.09, Ushant: 0.19±0.08.)

There was a fairly consistent increase in `Fc` and `Fvalid` from 1990 to 2010 (Figure 3). Anomalies became positive at both fronts in the middle of the time series, around 2001. However, since 2005 the trend stagnated and there was even a slight decrease in `Fc` and `Fvalid` in the late 2000’s. Notable lows in `Fc` and `Fvalid` coincided with the high `Fprob` and low `Fmean` years of 1990 and 1996. The relationship between the observed increase in `Fc` and interannual variability of `Fprob` and `Fmean` is described in the following section 3.22.

Seasonal patterns for `Fprob` differed between the Celtic Sea and Ushant Front (Figure 4). `Fprob` values at the Ushant Front were decreasing until April, became positive in June and did
not drop to negative until December. At the Celtic Sea Front, seasonal fluctuations of $F_{prob}$ were more variable. Anomalies were positive during the summer from June to September, negative between October and November, positive again until February and again negative until June (Figure 4). The positive $F_{prob}$ anomalies during the winter months, when tidal mixing fronts are absent, indicate the inclusion of frontal segments that are not the focus of this study. In this case, this unwanted signal was likely introduced by parts of a coastal current that runs along the east coast of Ireland. By restricting the sampling subset to 12km away from the coasts, it was anticipated to exclude coastal influences, which was clearly not sufficient. $F_{mean}$ displayed a typical seasonal curve at both fronts with increasing values from the beginning of the year until August/September and a sharp decrease thereafter.

$F_{clear}$ and $F_{valid}$ exhibited typical seasonal cycles, similar to the one seen for $F_{mean}$ (Figure 4). Positive anomalies of $F_{valid}$ occurred from May to September at the Celtic Sea Front and May to October at the Ushant Front. Anomalies of $F_{clear}$ were positive throughout March to September at both fronts. However, $F_{clear}$ values dropped notably in July and increased slightly again thereafter.
Figure 3 (colour): Yearly anomalies of $F_{prob}$, $F_{mean}$, $F_{clear}$ and $F_{valid}$ at the Celtic Sea and Ushant Front from 1990 to 2010. Anomalies are based on a seasonal subset (March to November). Blue bars represent negative anomalies and red positive anomalies. Black line represents loess smoother ($\alpha = 0.6$).
3.2 Effect of $F_{clear}$ on variability of $F_{prob}$ and $F_{mean}$

Preliminary analyses indicated a correlation between $F_{clear}$ and the two metrics $F_{prob}$ and $F_{mean}$. The temporal pattern seen for $F_{prob}$ and $F_{mean}$ might not purely be a result of changes in meteorological or hydrodynamic forcing over seasonal and interannual cycles, but caused to a certain degree by variations in available data. To investigate an effect of $F_{clear}$ on temporal variability of $F_{prob}$ and $F_{mean}$, inter-annual and seasonal variability of both metrics were modelled including $F_{clear}$ as an explanatory variable. In a follow up analysis, which is not presented here, temporal variability of these fronts was investigated in relation to meteorological factors known to influence frontal dynamics (e.g. heat flux, wind speed), but which are also partly correlated with $F_{clear}$ (Suberg, 2015). However, an $F_{clear}$
effect remained even when accounting for atmospheric forcing and can therefore, not be explained by covariability with meteorological factors alone. For brevity purposes, this analysis focuses on $F_{\text{clear}}$ only.

There was also a significant effect of $F_{\text{clear}}$ on $F_{\text{prob}}$ (Figure 5 and Table 3). The relationship was negative and levelled off at higher $F_{\text{clear}}$ values (Figure 6). The inclusion of $F_{\text{clear}}$ caused a notable modification of the interannual pattern of $F_{\text{prob}}$. The model accounting for $F_{\text{clear}}$ did not suggest significant interannual variability in $F_{\text{prob}}$ at the Celtic Sea and Ushant Front, whereas a model without $F_{\text{clear}}$ suggests a negative trend over time (Figure 6, red lines). In addition, the seasonal curve of $F_{\text{prob}}$ was more distinct when accounting for $F_{\text{clear}}$ and showed the expected pattern with higher $F_{\text{prob}}$ values in summer and lower values during the winter, when tidal mixing fronts are absent.

The relationship between $F_{\text{clear}}$ and $F_{\text{mean}}$ at both fronts was very strong and overall, positive (Figure 6 and Table 3). The relationship was stronger at the lower value range of $F_{\text{clear}}$ and levelled off with increasing $F_{\text{clear}}$ (Figure 6). In consequence, accounting for $F_{\text{clear}}$ resulted in changes in the interannual pattern of $F_{\text{mean}}$. The decrease at the beginning of the time series was stronger and the increase in the second half was less steep compared to the pattern seen in Figure 3. When $F_{\text{clear}}$ was not included in the model, the relationship between $F_{\text{mean}}$ and time was positively linear (Fig. 6, red lines). Although the model fit should be interpreted with caution as it appears to be an oversimplification of the real relationship. Not accounting for $F_{\text{clear}}$ results generally in a less steep drop at the beginning of the time series, followed by a stronger increase than. Seasonal variability on the other hand, was not greatly affected by $F_{\text{clear}}$ and still displayed the seasonal cycle and timing as seen in Figure 4. While factors $F_{\text{clear}}$ and months explained considerable amount of the variability, year only lead to a 0.03/0.04 (Celtic Sea/Ushant) increase in the model $R^2$ (Table 3). A summary of the effect of $F_{\text{clear}}$ on temporal variability of $F_{\text{prob}}$ and $F_{\text{mean}}$ is given in Table 4.

**Table 3:** Summary of GAMMs with AR1 structure for a seasonal subset of $F_{\text{prob}}$ and $F_{\text{mean}}$ (March/April to November) anomalies for Celtic Sea and Ushant Front modelled as a function of year, month and $F_{\text{clear}}$ (coefficients for model including $F_{\text{clear}}$ shown in black, model without $F_{\text{clear}}$ shown in red). Only significant covariates are listed, including their estimated degrees of freedom (edf), $F$-values, $p$-values and reduction in AIC. The adjusted $R^2$ for the final model is given in bold (Adj.$R^2$) and increase for each additional variable.

| Metric | Front | Covariate (edf) | $F$-value | $p$-value | $\Delta$-AIC | Adj. $R^2$ |
|--------|-------|-----------------|-----------|-----------|--------------|------------|

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Figure 5: GAMM predictions showing temporal variability (year and month) of $F_{prob}$ anomalies with (black) and without (red) accounting for $F_{clear}$ and the relationship between $F_{prob}$ and $F_{clear}$. An AR1 structure was added to the GAMM to account for temporal autocorrelation. The model is based on a seasonal subset of $F_{prob}$ (March/April to November, $N=189/168$). Upper panel shows Celtic Sea Front, lower panel Ushant Front. Solid lines represents fitted values, dotted lines 95% confidence intervals. Note: factor “year” was insignificant for the inclusive $F_{clear}$ model (black lines) and is not shown in table 3.
Figure 6: GAMM predictions showing temporal variability (year and month) of $F_{mean}$ anomalies with (black) and without (red) accounting for $F_{clear}$ and the relationship between $F_{mean}$ and $F_{clear}$ at the Celtic Sea Front and Ushant Front. An AR1 structure was added to the GAMM to account for temporal autocorrelation. The model is based on a seasonal subset of $F_{mean}$ (March/April to November, $N=189/168$). Upper panel shows Celtic Sea Front, lower panel Ushant Front. Solid lines represents fitted values, dotted lines 95% confidence intervals.

Table 4: Summary table of the significance of the number of clear pixels and its effect on inter-annual and seasonal variability of $F_{mean}$ and $F_{prob}$ at both fronts Celtic Sea and Ushant Front.

| Metric | Front         | Effect of $F_{clear}$ |
|--------|---------------|-----------------------|
|        | Celtic Front  |                       |
| $F_{prob}$ |                | Significance: Yes (negative correlation)  |
|         |                | Inter-annual variability: Strong effect  |
|         |                | Seasonal variability: Weak effect       |

|        | Ushant Front  |                       |
|        |                | Significance: Yes (negative correlation)  |
|         |                | Inter-annual variability: Strong effect  |
|         |                | Seasonal variability: Weak effect       |

|        | Celtic Front  |                       |
|        |                | Significance: Yes (positive correlation)  |
|         |                | Inter-annual variability: Strong effect  |
|         |                | Seasonal variability: Weak effect       |

|        | Ushant Front  |                       |
|        |                | Significance: Yes (positive correlation)  |
|         |                | Inter-annual variability: Strong effect  |
|         |                | Seasonal variability: Weak effect       |
4 Discussion

This research uses time-series analyses of two seasonal shelf-sea fronts as a framework for the first coherent guide on the use of satellite-derived frontal metrics in quantitative analyses. The results of the study will be discussed in the context of managing frontal metrics in quantitative analyses.

4.1 Recommendations on the metric for temporal analyses

$F_{prob}$ and $F_{mean}$ describe two distinct characteristics of a front (probability versus strength) and consequently, display specific and independent temporal pattern. It is important to keep in mind that the two metrics are complementary and both are required in order to describe a frontal feature thoroughly. Therefore, we recommend the combined use of both metrics to investigate differences in temporal pattern and relationships with other (e.g. environmental) variables for each metric.

Results of this study concur with previous research and support the suitability of $F_{prob}$ and $F_{mean}$ for temporal variability studies. The seasonal cycles of $F_{prob}$ and $F_{mean}$ are in agreement with the onset and breakdown of stratification in the Celtic Sea and previous observations of the Celtic Sea and Ushant Fronts (Eliot and Clarke, 1991; Pingree, 1975; Young et al., 2004). Model simulations of stratification in the Celtic Sea predict the thermocline to establish around the Celtic Deep first (near the Celtic Sea Front) around April, advancing over the shelf and reaching the Western English Channel (location Ushant Front) within a month. The delay in frontal development between the Ushant and Celtic Sea Front was also indicated by the satellite data (Figure 4, 5 and 6). Interesting to note is furthermore, the seasonal curve for $F_{mean}$ being slightly sharper than the one for $F_{prob}$. Once the fronts are established (June to August for the Celtic and July to September for the Ushant Front), frontal probability remains fairly stable, whereas the frontal strength consistently changes in response to decreasing and increasing temperatures/stratification.

Inter-annual pattern of $F_{prob}$ showed abnormally high values (and low values in $F_{mean}$) in 1990 and 1996. These extremes are partially caused by confounding factors, such as higher than usual cloud cover, which led to a reduction of available satellite imagery. Other explanations will be discussed in the next section (4.2). Apart from these extremes, no obvious changes in $F_{prob}$ occurred over the study period. The results of the long-term analysis suggest that the strength of the frontal temperature gradient ($F_{mean}$) oscillated...
between 1990 and 2010 at both fronts (Figure 6). Oscillations in frontal strength are expected in response to meteorological forcing (Holt et al., 2010). In a follow up analysis, which investigates the underlying drivers of the observed temporal variability, SST and net heat flux were found to be the predominant meteorological factors explaining the variation in $F_{\text{mean}}$ (Suberg, 2015). An increase in SST in the study area could have caused the observed intensification of $F_{\text{mean}}$ over the later ten years of the time series. Modelling studies predict tidal mixing fronts in the Celtic Sea to intensify due to increasing water temperatures during this century (Holt et al., 2010; Marsh et al., 2015).

$F_{\text{comp}}$, $F_{\text{pers}}$ or $F_{\text{dens}}$ were not analysed in detail here to their high correlation with $F_{\text{prob}}$ and/or $F_{\text{mean}}$. This is essentially due to the fact that $F_{\text{prob}}$ and $F_{\text{mean}}$ are base metrics for describing frontal characteristics and all other metrics are derivates of either one or both. In general, we recommend the use of $F_{\text{prob}}$ and $F_{\text{mean}}$ for temporal analysis over $F_{\text{comp}}$, $F_{\text{pers}}$ or $F_{\text{dens}}$, because the later complicate interpretation without providing additional information. $F_{\text{pers}}$ could serve as a synthesis of both $F_{\text{mean}}$ and $F_{\text{prob}}$, but with some restrictions as it can be dominated by either one of the two components. $F_{\text{comp}}$ and $F_{\text{dens}}$ represent slightly more contrasted versions of $F_{\text{pers}}$ and are quite suitable for visualization purposes or a synthetic spatial analysis, because they allow for clearer distinction between low and high frontal frequency areas.

### 4.2 Effect of data quantity on frontal metrics

$F_{\text{clear}}$ had significant, but contrasting effects on the temporal pattern of $F_{\text{prob}}$ and $F_{\text{mean}}$. Overall, the relationship between $F_{\text{clear}}$ and $F_{\text{mean}}$ was positive, but levelled out at high numbers of clear pixels. More clear pixels will lead to more cloud free scenes and subsequently, a higher detection rate of frontal segments. In addition, indirect factors increase the relationship between $F_{\text{mean}}$ and $F_{\text{clear}}$. Stronger temperature gradients across tidal mixing fronts are likely to be correlated with summer months or good weather periods with less cloud cover, stronger solar irradiance and higher temperatures. Under these conditions, tidal mixing fronts will strengthen or develop quicker (Holt et al., 2010; Young et al., 2004). At the same time, summer months and decreased cloud cover are also linked to higher $F_{\text{clear}}$. Therefore, it is essential to account for data quantity when using $F_{\text{mean}}$ for quantitative analyses. $F_{\text{mean}}$ has not been widely used in time series analysis and comparisons with other studies are not possible.

In contrast to $F_{\text{mean}}$, the relationship between $F_{\text{prob}}$ and $F_{\text{clear}}$ in the lower value ranges was negative. The reason for the negative correlation is that $F_{\text{prob}}$ is a simple proportion
between valid and clear pixels ($F_{\text{valid}}$ and $F_{\text{clear}}$). There was a strong positive correlation between $F_{\text{valid}}$ and $F_{\text{clear}}$ ($r=0.8$) and a notable increase over time for both. In addition, years with notably low $F_{\text{clear}}$, and for that matter low $F_{\text{valid}}$ (e.g. 1990 and 1996), showed disproportionally high $F_{\text{prob}}$ values. This contradictive pattern is due to a divisor effect. Over the time frame of this research, the increase in number of satellites has led to an increase in the number of clear pixels ($F_{\text{clear}}$), which was much higher than the increase in the number of front pixels ($F_{\text{valid}}$). For example, from the first five years of the time series (1990-1994) the average number of front pixels in a given location (pixel) increased from 0.97±0.42 to 1.91±0.86 in the last five years (1996-2010) at the Celtic Sea Front (Ushant: from 0.88±0.45 to 1.56±0.9), whereas clear pixels have risen from 11.62±6.15 to 30.75±13.38 (Ushant: from 10.7±6.55 to 27.28±15.22). This represents a 2.65-fold increase in clear pixels (Ushant: 2.55), but only a 1.97-fold increase in front pixels (Ushant: 1.77). Therefore, the number of front pixels is divided by an increasingly higher number of clear pixels over time, which results in a decrease of $F_{\text{prob}}$ ($F_{\text{prob}} = F_{\text{valid}}/F_{\text{clear}}$). The average $F_{\text{prob}}$ for 1990-1994 was 0.08 compared to 0.06 between 2006 and 2010 at both fronts. According to this, frontal probability has decreased by 25% from the first to the last quarter of the time series, which is unlikely and not supported by any other studies concerning interannual variability of $F_{\text{prob}}$ (e.g. Belkin et al., 2005; Kahru et al., 2012).

The $F_{\text{clear}}$ effect also adds to the high $F_{\text{prob}}$ values observed during winter. Tidal mixing fronts are absent during this time of the year and the high $F_{\text{prob}}$ indicates, on the one hand, the inclusion of signals from wintertime fronts, which will be discussed in section 4.3. However, the signal was much lower in $F_{\text{mean}}$. It is likely that higher cloud cover during winter leads to fewer clear pixels and hence, $F_{\text{valid}}$ being divided by a smaller number of $F_{\text{clear}}$, which resulted in an elevated $F_{\text{prob}}$, while $F_{\text{mean}}$ was not affected by the divisor effect.

The relationship between $F_{\text{prob}}$ and $F_{\text{clear}}$ has largely been ignored in the majority of research that uses satellite imagery to investigate temporal variability of fronts (e.g. Belkin et al., 2005; Kahru et al., 2012) and only been mentioned in a couple of studies (Obenour, 2013; Oram et al. 2008; Ullman et al., 2007). Oram et al. 2008 note that the increase in available satellite images during the second half of their study (1997-2002) caused bias in their detection probabilities ($F_{\text{prob}}$). Ullman et al. (2007) suggested that the non-linear relationship between clear and front pixels is caused by the failure of the SIED-algorithm to identify all frontal pixels as such, particularly in partially cloud-covered scenes. The clouds block the contour-following part of the SIED algorithm, resulting in $F_{\text{prob}}$ being underestimated. Obenour (2013) suggests the SIED-window should be at least 90% cloud-free during image
processing in order to avoid exactly this problem and subsequently, avoid temporal variability of $F_{prob}$ caused by the fraction of clear pixels. Obenour (2013) addresses the $F_{clear}$ effect by increasing data quality at the expense of data quantity: that approach differs to the one used in this study, which accounts for the amount of clear pixels during the statistical analysis stage, regardless of the difficulties caused by partially cloudy scenes.

Most temporal variability studies focus on seasonal variability and did not report any discontinuities of $F_{prob}$ caused by $F_{clear}$ (e.g. Castelao et al., 2014; Hickox et al., 2000; Mavor et al., 2001). However, the $F_{clear}$ effect appears to be less obvious when investigating seasonal variability, as seen in this study. Less research has focused on interannual patterns and mostly reported an increase in $F_{prob}$ over time. For example, Belkin and Cornillon (2005) found a surprising 50% rise in the annual mean of $F_{prob}$ between 1985-96, averaged over the entire Bering Sea. Similarly, Kahru et al. (2012) showed a significant increase in $F_{prob}$ in the California Current System over 29 years (1981-2009). However, both studies did not consider the changes in available data. Ullman et al. (2007) used frontal maps from 1985 to 2001 to investigate temporal and spatial variability of $F_{prob}$ in four regions of the North Atlantic. They mentioned the dependency of $F_{prob}$ on $F_{clear}$, which could lead to an underestimation of $F_{prob}$. However, they concluded that it did not influence their results, because seasonal peaks of $F_{clear}$ did not coincide with peaks in $F_{prob}$. In this research the seasonal pattern between $F_{prob}$ and $F_{clear}$ were not identical either, showing different seasonal peaks, but the relationship became evident only during the modelling process.

Therefore, Ullman et al. (2007) might have underestimated the effect of $F_{clear}$. Obenour (2013) is the only study to our knowledge that accounts for the clear pixel issue in their analyses, using the method described above (SIED-window >90% cloud free). Despite accounting for $F_{clear}$, Obenour (2013) still found an overall increase in global $F_{prob}$ from 1981 to 2011, which varied between different (selected) regions of the world.

Although most of these studies did not account for $F_{clear}$, they generally report a rise in $F_{prob}$ over time. Direct comparisons between this study and previous research are difficult, because of different study locations (e.g. California Current System, Bering Sea), study periods and durations, and the fact that these studies combine distinct fronts by spatially averaging over large areas. Subsequently, winter and summer time fronts, which may have different long-term trend pattern, are merged. For example, Belkin and Cornillon (2005) use frontal maps from before 1995, a period when the increase in satellite imagery was not as marked. It is possible that a divisor effect in other parts of the world is not as significant because of different weather patterns and cloud cover throughout the year. It is also possible
that in this research the effect of $F_{clear}$ has been overestimated by the statistical model, masking genuine temporal variability in the other metrics.

In summary, the effect of $F_{clear}$ on $F_{prob}$ and $F_{mean}$ is strong and the amount of available data should always be considered in any analysis. Because of the non-linear relationship between $F_{clear}$ and $F_{prob}/F_{mean}$, not all variability will be removed when accounting for $F_{clear}$ and variability relating to actual changes in frontal occurrence can still be observed. In addition, $F_{clear}$ is mostly an issue in the lower value ranges. Therefore, one could use data above a certain $F_{clear}$ threshold only (determined via statistical analysis on the given dataset) and make the assumption that all the variability observed is actually due to changes in the frontal structure. It clearly requires more investigations on how to best account for an $F_{clear}$ effect. A combined approach appears sensible, whereby an $F_{clear}$ effect is reduced during frontal map processing (Obenour, 2013) and subsequently, tested for during statistical analysis (this research).

4.3 Importance of differentiating between distinct types of fronts

High values of $F_{prob}$ were found during winter at the Celtic Sea Front, which were likely frontal segments not belonging to the front of interest, but to a coastal current. The inclusion of this signal affects the results of temporal analyses, because it adds variability independent of the front of interest. Different types of fronts respond to atmospheric and hydrodynamic forcing in specific ways and subsequently, display a distinct spatio-temporal variability (Hickox et al., 2000). When summarising frontal activity over large areas, e.g. entire seas, fronts with different temporal variability pattern will be combined and their individual temporal signals blurred. Therefore, it is difficult to draw meaningful conclusions about frontal activity from a cumulative temporal signal obtained over large areas.

It would make sense for any type of temporal analyses, seasonal or trend, to separate distinct types of fronts. In addition, individual fronts or particular types often play a specific role in oceanographic or biological processes and their effect on the ecosystem can vary (Scales et al., 2014). It is therefore of interest for ecologists and oceanographers alike to be able to distinguish between individual features and study them in isolation. Isolating features of interest is difficult, particularly in areas with high frontal activity, where various fronts exist in close proximity and often merge, such as shelf-seas (Achta et al 2015). In this research, the study area was refined by resampling different sized subsets (see supplement 6.1). Although the process was parameterized as much as possible, there is some arbitrariness and the possibility of unwanted features entering the study region. A newly developed technique,
called synoptic front maps, could prove useful for isolating fronts for analysis. It is based on a novel line-clustering algorithm, which first involves smoothing the $F_{\text{mean}}$ map with a Gaussian, then the most prominent frontal observations and directions are identified and followed to generate contiguous contours. This front simplification algorithm is in preparation for publication (Miller, in preparation).

### 5 Conclusions

Frontal maps were initially developed to visualise fronts, using image processing algorithms to detect, identify and enhance frontal features. However, for statistical analysis the user should be aware of their qualities and limitations. This guide on frontal metrics highlights essential points to think about before and during the analysis stage. Metrics belonging to the group $F_{\text{prob}}$, $F_{\text{pers}}$, $F_{\text{comp}}$ were highly correlated, whereas $F_{\text{mean}}$ and $F_{\text{dens}}$ displayed weaker correlations with other metrics. We recommend using $F_{\text{prob}}$ for temporal analysis of frontal persistence and $F_{\text{mean}}$ for frontal strength; the more complex metrics hinder interpretation without adding information. However, for visual analysis, frontal maps based on complex metrics (e.g. $F_{\text{dens}}$, $F_{\text{comp}}$) may be more appropriate, because they highlight persistent features and suppress transient segments that add noise to the maps. Although this appears to make the use of complex metrics in spatial analysis more desirable, e.g. in ecology to explain animal distribution, we still recommend the use of interpretable metrics such as $F_{\text{prob}}$ and $F_{\text{mean}}$. Alternatively, a combination of metrics (complex, but spatially clean versus simple and noisy, but interpretable) can be used to entangle the relationship between fronts and animal distribution. Secondly, data quantity has to be accounted for as it can introduce spurious trends: $F_{\text{prob}}$ and $F_{\text{mean}}$ were strongly affected by $F_{\text{clear}}$. A combination of improving data quality during the data processing stage as well as including $F_{\text{clear}}$ as a factor in statistical models is recommended. We used frontal maps at monthly resolution and focused on a specific type of front in this research. It would be useful to investigate the $F_{\text{clear}}$ effect on fronts in other regions, on other types of fronts and at higher temporal resolutions. For example, frontal types other than tidal mixing fronts, which are not subject to meteorological factors (which tends to covary with $F_{\text{clear}}$) as much could be less sensitive to $F_{\text{clear}}$. Finally, depending on the research question, scientists should consider studying individual fronts in isolation to avoid blurring of signals due to contrasting temporal food prints of different frontal types.

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