Inelastic light scattering by 2D electron system with SO interaction

Alexander V Chaplik\(^1,2\), Lev I Magarill\(^1,2\)* and Ritta Z Vitlina\(^1\)

Abstract

Inelastic light scattering by electrons of a two-dimensional system taking into account the Rashba spin-orbit interaction (SOI) in the conduction band is theoretically investigated. The case of resonance scattering (frequencies of incident and scattered light are close to the effective distance between conduction and spin-split-off bands of the A\(_{III}\)B\(_{V}\)-type semiconductor) is considered. As opposed to the case of SOI absence, the plasmon peak in the scattering occurs even at strictly perpendicular polarizations of the incident and scattered waves. Under definite geometry, one can observe the spectrum features conditioned by only single-particle transitions. In the general case of elliptically polarized incident and scattered light, the amplitude of the plasmon peak turns out to be sensitive to the sign of the SOI coupling.

Keywords: Two-dimensional system, Inelastic light scattering, Spin-orbit interaction, Rashba model

Background

It is well known that the spectrum of light scattering by a two-dimensional (2D) electron system is characterized by two contributions. One of them is determined by charge density excitations which is commonly called screened scattering. The shift of frequency equals the 2D plasmon frequency. The maximum of intensity of the corresponding peak in light scattering is reached when polarizations are parallel, and it is equal to 0 when polarizations are perpendicular.

The other contribution corresponds to single-particle excitations (SPE). The typical frequency shift is of the order \(qv_F\), where \(q\) is the wave vector transfer and \(v_F\) is the Fermi velocity. The intensity of this peak is maximal for perpendicular polarizations of the incident and scattered waves. As to polarized scattering, the SPE contribution strongly depends on the resonance parameter (see [1]): if the incident frequency is close to the effective bandgap (including the Moss-Burstein shift), the SPE peak can be comparable with the plasmon one.

The SOI substantially changes the spectrum of inelastic light scattering. A new peak (of a nontrivial shape) appears with the frequency shift equal to the spin splitting at the Fermi momentum. The polarization dependences are changed qualitatively. The plasmon peak can occur even at crossed polarizations. Finally, the left to right symmetry of circularly polarized incident light is violated: the cross section is invariant under simultaneous change of signs of polarizations and the SOI constant. This allows, in principle, to determine the sign of the Rashba constant experimentally.

Methods

Expressions for the scattering cross section

In the random-phase approximation, the differential cross section for the scattering by a 2D system can be written as follows [2-4]:

\[
\frac{d^2\sigma}{d\omega d\Omega} = \frac{\omega_2}{\omega_1} \left( \frac{e}{c} \right)^4 n_\omega + \frac{1}{\pi} \text{Im} \left( L_2 - \frac{2\pi e^2 L_1 L_1}{q_k} \right),
\]

(1)

where \(L_2\), \(L_1\), and \(\tilde{L}_1\) are respectively given by the expressions

\[
L_2 = \frac{1}{S} \sum_{\beta'\beta} |\gamma_{\beta'\beta}|^2 F_{\beta'\beta}, \quad L_1 = \frac{1}{S} \sum_{\beta'\beta} \gamma_{\beta'\beta}^* F_{\beta'\beta} F_{\beta'\beta},
\]

\[
\tilde{L}_1 = \frac{1}{S} \sum_{\beta'\beta} \gamma_{\beta'\beta}^* F_{\beta'\beta} (q) F_{\beta'\beta},
\]

(2)
Here, \( \omega_{1,2} \) are the incident and scattered light frequencies, respectively; \( q = q_1 - q_2 \), \( q_{1,2} \) are the in-plane components of the incident and scattered light wave vectors, respectively; \( \omega = \omega_1 - \omega_2 \) is the frequency shift in the inelastic light scattering; \( n_\omega = 1/(e^{\omega/T} - 1) \) is the Bose distribution function; \( J(q) = e^{iqr} \), \( \beta \) is the set of quantum numbers characterizing an electron state in the conduction band; \( S \) is the normalization area; \( \kappa \) is the background dielectric constant; \( \gamma \) is the scattering operator; and \( h = 1 \) is assumed throughout this paper. The longitudinal dielectric function of electrons in the conduction band \( \epsilon \) has the form

\[
\varepsilon(\omega, q) = 1 + \frac{2\pi e^2}{q\kappa} \frac{1}{S} \sum_{\beta' \beta} |F_{\beta' \beta}|^2, \tag{3}
\]

\[
F_{\beta' \beta} = \frac{f_{\beta'} - f_{\beta}}{(\omega + \varepsilon_{\beta' \beta} + i\delta)}, \quad (\delta = +0), \tag{4}
\]

where \( f_{\beta} \equiv f(\varepsilon_{\beta}), f(\varepsilon) \) is the Fermi distribution function, \( \varepsilon_{\beta} \) is the energy of an electron in the conduction band, and \( \varepsilon_{\beta' \beta} = \varepsilon_{\beta} - \varepsilon_{\beta'}. \)

The resonant situation is considered when the frequencies of incident (scattered) wave \( \omega_1 (\omega_2) \) are close to \( E_0 + \Delta_0, \) i.e., resonance with the spin-orbit split-off band takes place \( (E_0 \) and \( \Delta_0 \) are the band parameters of the bulk A_{111}B_{11} \) semiconductor). In this case, the operator of scattering \( \gamma \) reads

\[
\gamma = \gamma_1 + \gamma_2 = A((ie_1 e_2^*) + i(\sigma a))/(q), \quad A = \frac{1}{2} \frac{p^2}{E_g - \omega_1}, \tag{5}
\]

where \( E_g \) is the effective bandgap width, \( a = [e_1, e_2^*], P \equiv p_{e\sigma}/m_e \) is the Kane parameter, \( e_{1,2} \) are the polarizations of incident and scattered photons, and \( \sigma \) are the Pauli matrices. We treat here the enhanced resonant factor \( A \) in Equation 5 just as a constant that is true for not extremely resonant regime: the denominator in Equation 5 is much larger than the Fermi energy of electrons. We do this in order to simplify calculations because our main goal in this paper is to demonstrate the qualitatively new features of the scattering process due to spin-orbit interaction.

The substitution of Equation 5 into Equation 1 yields an expression comprising four characteristic contributions to the scattering:

\[
\frac{d^2\sigma}{d\omega d\Omega} = \frac{\omega_2}{\omega_1} \left( \frac{e}{c} \right)^4 \frac{n_\omega + 1}{\pi} R(\omega), \quad R(\omega) = \sum_{j=1}^{4} R_j(\omega), \tag{6}
\]

where

\[
R_1(\omega) = A^2 k q \left| \frac{1}{i} \right|^2 \text{Im} \left( \frac{1}{\epsilon} \right), \tag{7}
\]

\[
R_2(\omega) = \frac{1}{5} \sum_{\beta' \beta} |(\gamma_2)_{\beta' \beta}|^2 \text{Im}(F_{\beta' \beta}), \tag{8}
\]

\[
R_3(\omega) = -\frac{2\pi e^2}{q\kappa} \text{Im} \left( \frac{E_g^2}{\epsilon} \right), \tag{9}
\]

\[
R_4(\omega) = A \text{Im} \left( \frac{1}{\epsilon} \right) \left( \frac{(e_1 e_2^*) Z + (e_1^* e_2) \tilde{Z}}{Z^2} \right). \tag{10}
\]

The values of \( Z \) and \( \tilde{Z} \) are given by expressions for \( L_1 \) and \( \tilde{L}_1 \) in Equation 2 with \( \gamma \) replaced by \( \gamma_2. \)

The contribution \( R_1 \) determines the scattering of light by fluctuations of charge density. The value \( R_2 \) determines unscreened mechanism of scattering and corresponds to single-particle excitations. It can be shown that in the absence of SOI in the conduction band, the values of \( Z \) and \( \tilde{Z} \) and, respectively, \( R_3 \) and \( R_4 \) are equal to 0 identically.

Equations 7 to 10 are general. They are valid for any Hamiltonian, describing electron states in the conduction band. In this paper, we consider the light scattering for the so-called Rashba plane, namely 2D electron gas in the presence of SOI. Such a system is described by the Hamiltonian [5]

\[
\hat{H}_0 = \frac{p^2}{2m} + \alpha \sigma \cdot \{ p, n \}. \tag{11}
\]

Here, \( p \) is the 2D momentum of the electron, \( m \) is the effective mass, \( \alpha \) is the Rashba parameter, and \( n \) is the unit vector normal to the plane of the system. The spectrum of this Hamiltonian has the form

\[
\varepsilon_{\beta} = \frac{p^2}{2m} + \mu \alpha p, \quad \mu = \pm 1, \tag{12}
\]

where \( \beta = (p, \mu) \) and the parameter \( \mu = \pm 1 \) labels two branches of the spin-split spectrum. The wave functions of the Hamiltonian (Equation 11) are

\[
\psi_{p,\mu} = \frac{e^{ipr}}{\sqrt{2\pi}} \left( i \mu e^{-i\varphi} \right). \tag{13}
\]
Results and discussion

Numerical calculations

Equations 7 to 10, 12, and 13 were used for numerical calculations of scattering cross section as a function of frequency shift \( \omega \). They were carried out for 2D electron gas at temperature \( T = 0 \) in the scattering geometry when incident and scattered beams make a right angle and lie in the same plane (Figure 1). The structure InAs/GaSb with \( \alpha = 1.44 \times 10^6 \text{ cm/s}, m = 0.055 m_0, \) and \( \kappa = 15.69 \) was considered at the areal concentration \( n_s = 10^{11} \text{ cm}^{-2} \). The contributions \( R_1, R_3, \) and \( R_4 \) contain plasmon poles (zeros of \( \epsilon \)). To get finite results, it is necessary to introduce a finite damping. We replace \( \delta \) in Equation 4 by the relaxation frequency \( \nu = e/\mu m \) (\( \mu \) is the mobility).

If the polarizations of incident and scattered waves are strictly parallel (\( e_1 \parallel e_2 \)), the cross section is determined by only \( R_1 \). The spectrum of scattering has two peaks: the plasmon peak \( \omega_0(q) = v_F \sqrt{q/\kappa a_B} \) and the SOI-induced peak at \( 2\alpha p_F \). The dependence of the cross section on the frequency shift for both peaks is similar to the plasmon absorption and is given by Figure 2.

Let the geometry of scattering in such a way that incident and scattered waves are linearly polarized and, moreover, \( e_1 \perp e_2 \) and \( e_3 = 0 \). It can be realized, e.g., if incident and scattered beams are perpendicular and one of them is polarized in the incidence plane but the other is perpendicular to it. In this case, the spectrum demonstrates peculiarities due to only single-particle transitions (contribution \( R_2 \)): one peak near the frequency \( qv_F \) and another peak near the frequency \( 2\alpha p_F \). This case is demonstrated by Figure 3.

Due to SOI, the plasmon peak in the light scattering spectrum can occur even at strictly perpendicular polarizations of incident and scattered waves. It occurs when vector \( a \) has a nonzero projection onto axis \( y \) (axes \( z \) and \( x \) were chosen along vectors \( n \) and \( q \), respectively). The nonvanishing contribution to the cross section is due to the sum \( R_2 + R_3 \). This case is presented by Figure 4.

For the existence of the contribution \( R_4 \), polarization vectors \( e_1 \) and \( e_2 \) should be arbitrarily oriented with
respect to each other (neither parallel nor perpendicular). Besides, at least one of the waves should not be linearly polarized. When these conditions are justified and $R_4 \neq 0$, all other contributions ($R_1, R_2, R_3$) also exist. Herewith, due to the sensitivity of the contribution $R_4$ to the sign of the effective Rashba SOI $\alpha$ and to polarization vector phases, the total cross section of scattering also depends on these parameters. Therefore, measurements of inelastic light scattering can be, in principle, used for the determination of the sign of the constant $\alpha$. Figure 5 shows an example of the inelastic light scattering spectrum in the most interesting case when the incident wave has right or left circular polarization while the scattered one is linearly polarized at the angle $\pi/4$ to the incidence plane. It is seen that at $\alpha > 0$, the amplitude of the plasmon peak for left polarization is distinctly larger than that for right polarization. For $\alpha < 0$, the curves should be interchanged.

Conclusions
Thus, allowing SOI essentially (qualitatively) changes the spectrum of inelastic light scattering by a 2D electron system. It should be especially noted that in the absence of external magnetic field, the symmetry between left and right polarizations is violated.

Competing interests
The authors declare that they have no competing interests.

Authors' contributions
AVC, LIM, and RZV equally contributed in writing the manuscript and in performing the theoretical analysis. All authors read and approved the final manuscript.

Acknowledgements
This research has been supported in part by RFBR grant nos. 11-02-00730 and 11-02-12142.

Received: 16 July 2012 Accepted: 2 September 2012 Published: 28 September 2012

References
1. Das Sarma S, Wang DW: Resonant Raman scattering by elementary electronic excitations in semiconductor structures. PRL 1999, 83:816.
2. Blum FA: Inelastic light scattering from semiconductor plasmas in a magnetic field. Phys Rev B 1970, 1:1125.
3. Vasko FT, Raichev OE: Quantum Kinetic Theory and Applications: Electrons, Photons, Phonons. New York: Springer; 2005.
4. Ivchenko EL: Optical Spectroscopy of Semiconductor Nanostructures. Harrow: Alpha Science; 2005.
5. Bychkov YuA, Rashba EI: Properties of a 2D electron gas with lifted spectrum degeneracy. JETP Lett 1984, 39:78. [Pis'ma ZhETF 1984, 39:66].

doi:10.1186/1556-276X-7-537

Cite this article as: Chaplik et al.: Inelastic light scattering by 2D electron system with SO interaction. Nanoscale Research Letters 2012 7:537.