NEARLY PERIODIC FLUCTUATIONS IN THE LONG-TERM X-RAY LIGHT CURVES OF THE BLAZARS 
AO 0235+164 AND 1ES 2321+419

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ABSTRACT

We have performed a structure function analysis of the Rossi X-Ray Timing Explorer All-Sky Monitor data to search for variability in 24 blazars using data trains that each exceed 12 yr. Although 20 of them show nominal periods through this technique, the great majority of these “periods” are clearly related to yearly variations arising from the instrument. Nonetheless, an apparently real periodic component of about 17 days was detected for the blazar AO 0235+164 and it was confirmed by discrete correlation function and periodogram analyses. For 1ES 2321+419, a component of variability with a near periodicity of about 420 days was detected by all of these methods. We discuss several possible explanations for these nearly periodic components and conclude that they most likely arise from the intersections of a shock propagating down a relativistic jet that possesses a helical structure.

Key words: BL Lacertae objects: general – BL Lacertae objects: individual (AO 0235+164, 1ES 2321+419) – galaxies: active

1. INTRODUCTION

The characterization of variability timescales can provide information on the sizes and locations of the emission regions in active galactic nuclei (AGNs). Although Doppler-boosted emission from a relativistic jet provides a very reasonable explanation for the nonthermal spectra and small-scale radio morphology of the BL Lacertae (BL Lac) objects and flat spectrum radio quasars that are now usually called blazars (e.g., Blandford & Rees 1978; Urry & Padovani 1995), the question of just where in such jets the emission at different wavelengths arises remains somewhat uncertain (e.g., Marscher et al. 2008).

While one of the defining characteristics of blazars is extreme variability, periodic, or quasi-periodic contributions to the electromagnetic emission have not been clearly detected, or even claimed to be present, in the vast majority of blazars, although they certainly have been searched for. Probably, the best case for such, albeit impermanent, special variations is S5 0716+714, which once showed quasi-periodic variations on the timescale of 1 day, followed by a weaker indication of a variable component of about 7 days, over the course of an intensive month-long monitoring program. Quite remarkably, these fluctuations were present simultaneously in an optical and a radio band (Quirrenbach et al. 1991). On another occasion, quasi-periodicity with a timescale of 4 days seemed to be present in the optical band (Heidt & Wagner 1996). Five major optical outbursts between 1995 and 2007 seem to occur at intervals of ~3.0±0.3 yr (e.g., Raiteri et al. 2003; Foschini et al. 2006; Gupta et al. 2008b, and references therein). Very recently, Gupta et al. (2009) performed a wavelet analysis on the 20 best nights of over 100 high-quality optical data sets taken by Montagni et al. (2006). They found very high probabilities that S5 0716+714 had quasi-periodic components to its intranight variability on timescales from ~25 to ~73 minutes on several different nights.

Only one other blazar, OJ 287 (0851+203), seems to have shown periodic variations in its light curves over a range of timescales comparable to that for S5 0716+714. A 15.7 minute periodicity in 37 GHz radio observations was reported by Valt遣ja et al. (1985) for OJ 287. In optical bands, a 23 minute periodicity was claimed by Carrasco et al. (1985) and short-lived 32 minute periodicity was reported by Carini et al. (1992). Long-term optical data on OJ 287 have shown a periodicity of ~11.7 yr; detailed analyses in this case support the hypothesis that this source contains a binary system of supermassive black holes (SMBHs) and the major flares arise when the less-massive SMBH passes through an accretion disk surrounding the bigger one (e.g., Sillanpää et al. 1996; Valtonen et al. 2008).

A few other blazars may have shown significant periodicity in their flux variations. In the blazar PKS 2155–304, a quasi-periodicity around 0.7 days seemed to be present (Gupta et al. 2002). On four >60 ks X-ray observations of the quasar 3C 273 by the XMM-Newton satellite also appears to have a quasi-periodic component with a timescale of about 3.3 ks (Espaillat et al. 2008). A recent analysis of a 91 ks XMM-Newton observation indicated the presence of a ~1 hr periodicity in the narrow line Seyfert 1 galaxy RE J1034+396 (Gierlinski et al. 2008). Using long-term (and, unfortunately, very inhomogeneous) optical data on 10 radio-selected blazars, Fan et al. (2002) have used the Jurkevich method to claim detection of quasi-periodicity in nine of them, with putative periods in the range of 1.4–17.9 yr.

In Section 2, we discuss the X-ray data for 24 blazars stretching over more than 12 yr. The structure function (SF) analyses of these data are given in Section 3.1 and they yield possible quasi-periodicities for 20 of those objects; however, the great majority of those periods are either ~1 yr or harmonics of an annual period and must be assumed to be an observational artifact. The SFs of four objects showed periods significantly different from a year and we performed additional analyses of these data (Sections 3.2 and 3.3) which strongly support the presence of a quasi-period of ~17 days for AO 0235+164 and of ~240 days for 2321+419. These results provide the first good evidences for a nearly periodic component to X-ray blazar variability longer than a few hours. In Section 4, we discuss our results in terms of several mechanisms that could produce nearly
Table 1

| Object Name | Periodicity (days) | $\alpha_{1,000}$ | $\delta_{1,000}$ |
|-------------|--------------------|------------------|------------------|
| 1ES0145+138 | 365 ± 7            | +14' 02" 18'     | 42.6             |
| 3C 66A      | 369 ± 16           | +43' 02" 08'     | 38.8             |
| AO 2035+164 | 17 ± 1, 162 ± 4,   | +16' 36" 59'     | 41.8             |
|             | 275 ± 20           |                  |                  |
| S4 0954+658 | 336 ± 14           | +84' 32" 05'     | 42.3             |
| S5 0716+714 | 347 ± 18           | +71' 20" 36'     | 37.6             |
| PKS 0735+178| 347 ± 31           | +17' 42" 19'     | 41.8             |
| PKS 0829+046| 364 ± 5             | +04' 29" 39'     | 39.9             |
| ON 231      | 148 ± 19, 337 ± 26 | +02' 13" 58'     | 46.5             |
| 3C 273      | 391 ± 26           | +02' 03" 09'     | 43.1             |
| 3C 279      | 362 ± 26           | -05' 47" 22'     | 43.1             |
| BL 1320+084 | 337 ± 8            | +08' 10" 10'     | 43.3             |
| OQ 530      | 650, 910, 1300     | +54' 23" 14'     | 41.7             |
| PG 1553+11  | 363 ± 18           | +11' 11" 24'     | 31.5             |
| BL 1722+119 | 361 ± 26           | +11' 52" 16'     | 34.8             |
| 3C 371      | None detected      | +69' 49" 28'     | 38.0             |
| S5 2007+77  | None detected      | +77' 52" 43'     | 39.3             |
| BL Lac      | 313 ± 12           | +42' 16" 39'     | 36.0             |
| 3C 454.3    | 361 ± 3            | +16' 08" 54'     | 37.0             |
| 1ES 2321+419| 425 ± 10           | +42' 11" 19'     | 33.3             |
| 1ES 2344+514| None detected      | +51' 42" 18'     | 33.3             |

Note.

$^a$Percentage of negative data points.

periodic fluctuations and we obtain estimates for the central black hole (BH) masses in these blazars in the rather unlikely case that the observed fluctuations are fundamentally related to orbits of emission regions at the inner edges of accretion disks. Our conclusions are in Section 5.

2. DATA

We extracted 1 day average X-ray fluxes in the 1.5–12 keV energy range from the All-Sky Monitor (ASM) instrument on board the Rossi X-Ray Timing Explorer satellite (RXTE)$^4$ for the 24 blazars listed in Table 1, which gives their names and coordinates in the first three columns. This data cover the period 1996 January 1 through September 1 2008. These objects are all of the blazars in the list of Nieppola et al. (2006) for which data are available on the RXTE Web site; all of them are low- and intermediate-energy-peaked blazars. A description of the ASM and how light curves are obtained from it is given in Levine et al. (1996). In these lengthy data sets, we found that the source flux counts were given as negative on many days of observations, indicating that the source fluxes were then below the detection threshold of the ASM/RXTE. Such negative flux counts, or upper limits were omitted in our analysis. We first converted the ASM/RXTE fluxes, given in counts s$^{-1}$, into a Crab flux unit, using the relation 1 crab $= 75$ counts s$^{-1}$; then the flux of the source is converted into Janskys, using 1 crab = 2.4 $\times 10^{-11}$ W m$^{-2}$. The X-ray light curves for four of the blazars are presented in Figure 1.

Since the ASM is a survey instrument, and none of these blazars are usually among the brightest of X-ray sources, the typical signal-to-noise ratio (S/N; $\sim$1.5–3) is rather poor for each daily data point, though the S/N is usually substantially higher during the times when the fluxes are near their peaks. Still, the ASM is a unique X-ray instrument, in that it can provide a multiyear light curve of any reasonably strong source. Our analysis turns out to yield significant, nonartifactual, periods for only two of the 24 blazars, AO 0235+164 and 1ES 2321+419 (Section 3). Recently, it has been noticed that a small number of ASM sources have their nominal intensity modulated by the emission of a nearby galactic X-ray source (e.g., Kaur et al. 2007). However, the nearest other source to AO 0235+164 observed by ASM/RXTE$^5$ is separated by $\pm 4^\circ$, which is far enough away that it is highly unlikely to contaminate the flux from 0235+164. In the case of 2321+419, the nearest ASM source is separated by over $16^\circ$ and so definitely too far away to cause a contamination problem.

3. ANALYSES AND RESULTS

3.1. Structure Functions

Ordinary Fourier transform methods are not optimal in a search for periodicity in these blazar light curves because the samplings of these light curves are not exactly uniform. Nor can simple periodograms give useful results. Under these circumstances, an SF analysis is the best way to quantitatively determine any timescale of variation on unevenly sampled data sets, as these ASM measurements have become once we chose to discard the days with “negative” fluxes.

The first-order SF is related to the power spectrum density (PSD) and discrete correlation function (DCF) and is thus a powerful tool to search for periodicities and timescales in time series data (e.g., Simonetti et al. 1985; Gupta et al. 2008a, and references therein). The first-order SF for a data set, $a$, having uniformly sampled points is defined as

$$D_{1}^{i}(k) = \frac{1}{N_{1}^{i}(k)} \sum_{i=1}^{N} w(i) w(i+k) [a(i+k) - a(i)]^{2},$$

where $k$ is the time lag, $N_{1}^{i}(k) = \sum_{i=1}^{N} w(i) w(i+k)$, and the weighting factor $w(i)$ is 1 if a measurement exists for the $i$th interval, and 0 otherwise. Since the data in our case are quasi-uniform, we first calculated the differences squared for all pairs of data points and then averaged the samples into bins of one or a few days; measurements are taken to not exist for negative flux values.

Simply summarized, the behavior of the first-order SF will at first rise with time lag (after a possible plateau arising from noise). Following this rising portion, the SF will then fall into one of the following classes: (1) if no plateau exists, any timescale of variability exceeds the length of the data train; (2) if there are one or more plateaus, each one indicates a timescale of variability; and (3) if that plateau is followed by a dip in the SF, the lag corresponding to the minimum of that dip indicates a possible periodic cycle (unless such a dip is seen at a lag close to the maximum length of the data train, when it is probably an artifact).

SF analyses have been employed for quite some time in examining the nature of AGN variability. For example, using long-term radio observations of a sample of over 50 radio loud AGN, Hughes et al. (1992) reported that most of them showed some plateau in their SFs; the mean timescale they

$^4$ ASM/RXTE Web site: http://xte.mit.edu/ASM_lc.html

$^5$ http://xte.mit.edu/lcextret/asmsel.html
found for BL Lac objects was 1.95 yr while that for quasars was 2.35 yr. A recent extension of this analysis using SFs and other techniques also examined higher frequency radio data and found that small-flux density variations were often present on 1–2 yr timescales but larger outbursts were much rarer; no significant difference between AGN classes was detected (Hovatta et al. 2007). In a different band, SFs were calculated from a large number of intranight optical light curves for several blazars (Sagar et al. 2004) and for a group of both radio loud and radio quiet quasars as well as blazars (Stalin et al. 2005). Indications of preferred observed timescales of a few hours were found for some objects in each AGN class, and hints of quasi periods were found for the BL Lac 0851+202 and the core-dominated quasars 0846+513 and 1216+010; however, in none of these cases were more than two dips seen in the SF, so no confident claim of quasi-periodicity could be made based on those data sets and those SF analyses alone.

The nominal periodicities and approximate standard errors obtained from the SF analyses for the X-ray light curves of each blazar in our sample are given in the fourth column of Table 1 and the percentage of negative points is listed in the last column. We wish to stress that for no blazar have we found a dominant component with a precise period, but we will henceforth use the words “period” and “periodicity” to denote the strongest nearly periodic signals seen in these data sets where the upper limits are not included in the analysis. Most of these SF indicated periods are found as averages from at least two dips and hence standard errors can be obtained, but the period given for OQ 530 is estimated from a single dip and so no errors can be quoted. The great majority of the periods in Table 1 are very close to 1 yr. This is not surprising, as there has been a previous report of annual, as well as daily, satellite orbital period (96 minutes) and satellite precession period (53 days) variations found to be imposed on the ASM fluxes of binary X-ray sources (Wen et al. 2006). Detection of these periods presumably can be attributed to windowing effects arising from the satellite and will not be investigated further.

The SF of the entire \textit{RXTE} light curve of the blazar AO 0235+164 is plotted in the lower left panel of Figure 2, binned in 2 day intervals. This SF shows several significant dips, with the first at about 17 days and the second about 34 days, providing a hint for a periodic component of about 17 days. The displayed binning values were chosen for each source so that peaks and dips would be clearest, but they remain visible when different bin sizes are used. The lower left panel of Figure 3 displays the SF for 2321+419, binned in 4 days intervals; following an almost flat region consistent with noise out to about 50 days the deepest dips are at about 425 and 850 days but are rather broad. To see whether this hint of a period is genuine, we performed other analyses on the same data set (Sections 3.2–3.4).

In contrast to those two cases, the lower left panel of Figure 4 shows the SF for 3C 454.3 (binned over 8 days), for which the only periodicity indicated by multiple clear dips in the SF is at essentially 1 yr. This is typical of the SFs of 13 of the 24 cases, where the only clearly indicated period is 365 days within a 1σ error; in two other cases, S5 0454+844 and 3C 273, the best value of any period is essentially within 2σ of a year and in one case, BL 1320+084, it is roughly 3σ away. All of these nominal periodicities are almost certainly instrumental “windowing” effects, along with the essentially one-half year periodicities detected for AO 0235+164 and OJ 287. In four other cases, the SF yielded no plausible periodic signal. In the last four, most interesting, cases, periods not comparable to 1 yr
AO 0235+164

**Folded Light Curve**

**Structure Function**

**DCF**

**LS Periodogram (Period at Peak = 17.7 days)**

**Folded Light Curve**

**Structure Function**

**DCF**

**LS Periodogram (Period at Peak = 423.3 days)**

**Figure 2.** Evidence for a periodic component of $\sim 17$ days in the variability of AO 0235+164. The folded partial light curve is in the upper left panel and the SF (in arbitrary units) is in the lower left panel. The DCF is in the upper right panel and the spectral power density for an LSP is at the lower right, with the horizontal lines indicating false alarm probability, $p$, values.

**Figure 3.** As in Figure 2 for 1ES 2321+419, where the periodic component is at $\sim 423$ days.
of the time series, and $\sigma_a^2$ and $\sigma_b^2$ are their variances. The correlation function is binned after calculation of the UDCF. The DCF method does not automatically define a bin size, so several values need to be tried. If the bin size is too big, useful information is lost, but if the bin size is too small, a spurious correlation can be found. For example, we have found that a bin size of 10 days is good for 2321+419 but the minimum bin size of 1 day length was best for AO 0235+164 while 15 days was appropriate for 3C 454.3. Taking $\tau$ as the center of time bin and $n$ is the number of points in each bin, the DCF is found from the UDCF via

$$\text{DCF}(\tau) = \frac{1}{n} \sum \text{UDCF}_{ij}(\tau).$$

The error for each bin can be calculated using

$$\sigma_{\text{def}}(\tau) = \frac{1}{n-1} \left\{ \sum (\text{UDCF}_{ij} - \text{DCF}(\tau))^2 \right\}^{0.5}.$$  

A DCF analysis is frequently used for finding the correlation and possible lags between multifrequency AGN data where different data trains are used in the calculation (e.g., Villata et al. 2004; Raiteri et al. 2003; Hovatta et al. 2007, and references therein). When the same data train is used, there is obviously a peak at zero DCF indicating that there is no time lag between the two, but any other strong peaks in the DCF can indicate a periodicity. A disadvantage of this method is that it does not give an exact probability that a resulting peak actually represents a periodicity. The only way to investigate the internal reliability of the DCF method is to use simulations; however, we have not done so, instead verifying the DCF analysis by cross-checking the results by the SF and Lomb–Scargle periodogram (LSP; Section 3.3) methods.

The results of the DCF analysis for AO 0235+164, 1ES 2321+419, and 3C 454.3 are shown in the upper right panels of

Table 2

| Object Name  | SF (days) | LSP (days) | DCF (days) |
|--------------|-----------|------------|------------|
| AO 0235+164  | 17 ± 1    | 17.7 (p = 0.0294) | 17         |
| OQ 530       | 650, 1302, 910 | 960.4 (p = 0.0848) | None clear |
| BL Lac       | 313 ± 12  | 365.4 (p = 5.82e-7) | None clear |
| 2321+419     | 425 ± 10  | 423.2 (p = 0.00609) | 430        |

(or one-half year) were found. Table 2 lists these four blazars with the most plausible real periods in Column 1 and gives their SF identified periodicity ties in Column 2. Their partial light curves are those shown in Figure 1.

3.2. Discrete Correlation Functions

The DCF method was first introduced by Edelson & Krolik (1988) and it was later generalized to provide better error estimates (Hufnagel & Bregman 1992). The DCF is suitable for unevenly sampled data, which is the case in most astronomical observations. In our case, as we have discarded the nominally negative counts, the data become unevenly sampled. Here, we give only a brief introduction to the method; for details refer to Hovatta et al. (2007), and references therein.

The first step is to calculate the unbinned discrete correlation function (UDCF) using the given time series through (e.g., Hovatta et al. 2007)

$$\text{UDCF}_{ij} = \frac{(a(i) - \bar{a})(b(j) - \bar{b})}{\sqrt{\sigma_a^2 \sigma_b^2}},$$

where $a(i)$ and $b(j)$ are the individual points in the time series $a$ and $b$, respectively, $\bar{a}$ and $\bar{b}$ are, respectively, the means of the time series, and $\sigma_a^2$ and $\sigma_b^2$ are their variances. The correlation function is binned after calculation of the UDCF.
Figures 2–4, respectively. The plotted maximum values of the DCF lags plotted were chosen so as to avoid crowded points, but the same features are present in SFs extending to the full lengths of the data sets. The resulting periods for these blazars, along with the negative DCF results for OQ 530 and BL Lac, are given in the fourth column of Table 2.

3.3. Lomb–Scargle Periodograms

The LSP is another useful technique for searching time series for periodic patterns. This method has a good tolerance for missing values (e.g., Glynn et al. 2006), so it does not require any special treatment for gaps in the data and is thus quite suitable for nonuniform data trains. Therefore, the LSP method is frequently used by astronomers and has found use in other fields as well (e.g., Glynn et al. 2006). It also has the advantage of providing a p-value which specifies the significance of a peak. The LSP was first introduced by Lomb (1976) and later extended by Scargle (1982); somewhat later a more practical mathematical formulation was found (Press & Rybicki 1989). Here, we briefly describe the method and formulae. We used a publicly available R language code for LSPs. If \( N \) is the total number of observations, the LSP is defined at a frequency \( \omega_j \) as (Press & Rybicki 1989; Glynn et al. 2006)

\[
P(\omega_j) = \frac{1}{2\sigma^2} \left\{ \frac{\sum_{i=1}^{N} [a(t_i) - \bar{a}] \cos[\omega_j(t_i - \tau)]}{\sum_{i=1}^{N} \cos^2[\omega_j(t_i - \tau)]} + \frac{\sum_{i=1}^{N} [a(t_i) - \bar{a}] \sin[\omega_j(t_i - \tau)]}{\sum_{i=1}^{N} \sin^2[\omega_j(t_i - \tau)]} \right\},
\]

(5)

Here \( j = 1, \ldots, M \), where \( \tau \) is defined by

\[
\tan(2\omega_j \tau) = \frac{\sum_{i=1}^{N} \sin(2\omega_j t_i)}{\sum_{i=1}^{N} \cos(2\omega_j t_i)},
\]

(6)

and \( M \) depends on the number of independent frequencies, \( N_0 \), through \( M = N_0 \approx -6.363 + 1.193 N + 0.00098 N^2 \) (Press et al. 2002).

The LSP also provides the ability to test for the presence of more than a single frequency. We can define a range of frequencies to be tested in the R code for the LSP, and it yields the most significant peak and its significance level. In searching for some periodic behavior of a data set, we actually test the null hypothesis, or false alarm probability, that the given data train is nonperiodic at each frequency. If the probability that the peak value of the LSP is smaller than \( p \), the \( p \)-value, or probability of the null hypothesis that the observed peak in an LSP was found by chance, is (e.g., Glynn et al. 2006)

\[
p = 1 - (1 - e^{-x})^M.
\]

(7)

The smaller the \( p \)-value for a given peak, the higher its significance; the maximum limit that can reasonably specified for a \( p \)-value is 0.05, i.e., any peaks having \( p \)-values smaller than 0.05 are considered as significant.

Two difficulties usually arise while using such periodograms (e.g., Scargle 1982); the first is statistical and the other is spectral leakage. The statistical difficulty is mitigated by using large sample sizes which improves the S/N for possible period detection as this S/N is proportional to the number of data points and here we use thousands of points encompassing many cycles of each putative periodicity. Spectral leakage, or aliasing, involves leakage of power to some other frequencies that are actually not present in the data. A small presence of unevenness in the data spacing substantially reduces aliasing and astronomical data are typically irregular enough that aliasing is effectively eliminated. However, if the sampling is semiregular (intermediate between randomly and evenly spaced) significant leakage of periodogram power to the side lobes can occur. The usual way to minimize both statistical and leakage problems is to window or taper the data by smoothing in the spectral domain. But the disadvantage of smoothing is that the spectral values at different frequencies are no longer independent, and hence the joint statistical properties become more complicated. Since the unevenness in our X-ray data (after rejection of negative data points) can be best characterized as random, any leakages of power are expected to be small, and we need not smooth our data.

The results of our LSP analysis, showing the peaks of the normalized power spectral densities for AO 0235+164, 1ES 2321+419, and 3C 454.3, are shown in the bottom right panels of Figures 2–4, respectively. The resulting periods for the first two blazars, along with the negative results for OQ 530 and BL Lac and their false alarm probabilities, \( p \), are given in the third column of Table 2.

3.4. Nearly Periodic Variations in Two Blazars

For all of our sources we have apparent periodic variations present for several (at least five) cycles. We first performed the SF and DCF analyses for the light curves of all the sources using unbinned data. Since the data length is large, on these original plots of the SF and DCF the points were very crowded. To reduce the data crowding, we binned the data in a variety of ways and chose to display the results for lengthy portions of the data trains and for binning values that provide good clarity in each of the plots. The same features remain if the entire nonnegative data trains and different bin sizes are employed.

To make clearer the scatter about the nearly periodic components of the light curves, we have also plotted folded light curves based on the partial light curves in Figure 1 for AO 0235+164 and 1ES 2321+419 and on four cycles of the quasi-annual variation seen in 3C 454.3. These are displayed in the upper left panels of Figures 2–4. With a nominal period of 17 days the date of the zero phase on the plot for AO 0235+164 is MJD 50347. It would be very interesting to see if subsequent observations detect fluctuations with the same, or similar, periodicities.

Because of the large number of upper limits in all of the data sets, it must be noted that our neglecting those values in our analyses is problematic. For the DCF analysis an alternative, albeit still somewhat arbitrary, approach would be to include all such points but to set their values equal to zero. We did perform such analyses and in all cases no significant peaks other than at lags of zero were seen and so any information on periodicity was lost to this form of DCF. It is to a large extent because of the uncertainties induced by the many upper limits and poor individual S/N values that we consider our claimed variations to be nearly periodic and not overwhelmingly convincing.
4. DISCUSSION

4.1. Properties of the Blazars with Periodic Variability

The blazar AO 0235+164 has a redshift of $z = 0.94$ based on detection of emission lines (Nilsson et al. 1996). Since it was among the first objects to be classified as a BL Lac (Spinrad & Smith 1975) and it is a highly variable and rather bright source it has been extensively studied, with over 640 papers mentioning this source. Its fractional polarization is up to ~40% in both the visible and IR bands (e.g., Impey et al. 1982) and it is significantly variable from the radio to the X-ray bands on timescales ranging from less than an hour to many years (e.g., Ghosh & Soundararajaperumal 1995; Heidt & Wagner 1996; Fan & Lin 1999; Romero et al. 2000; Webb et al. 2000; Raiteri et al. 2001; Padovani et al. 2004; Sagar et al. 2004; Gupta et al. 2008b). Some of this fast variability is probably due to gravitational microlensing (e.g., Webb et al. 2000) as there are foreground absorbing systems at $z = 0.524$ and $z = 0.851$ (Burbridge et al. 1976).

Raiteri et al. (2001) used 25 yr of radio and optical data on AO 0235+164 to argue it seemed to have a long quasi period of ~5.7 yr, but the predicted outburst in 2004 was not detected (e.g., Raiteri et al. 2006). These authors then suggested an ~8 yr periodicity might be a better fit to the data. More recent optical observations provide some measure of support for that suggestion (Gupta et al. 2008b). Our analysis of the archival RXTE/ASM data provides the first claim for an X-ray periodicity for this popular blazar. Using scaling relations between low-frequency extended radio emission and high-frequency beamed emission (Giovannini et al. 2001), Wu et al. (2007) have determined a rough value of the Doppler factor for the relativistic jet of AO 0235+164 of $\delta \simeq 10.5$.

The other blazar that seems show a periodic component to the variability revealed by the RXTE/ASM data set is 1ES 2321+419 ($z = 0.059$; Padovani & Giommi 1995). This source is significantly fainter than AO 0235+164 in the optical band and has therefore received much less attention. Still, it has been studied since its X-ray detection (Elvis et al. 1992) in optical (e.g., Falomo & Kotilainen 1999) and radio (e.g., Kollgaard et al. 1996) bands and a spectral energy distribution is available (Nieppola et al. 2006). There have not been any sustained efforts to look for variability in this blazar in any wave band. A rather low estimate of $\delta \simeq 1.7$ is available (Wu et al. 2007).

4.2. Unlikely Explanations for Periodic Variability

The simplest explanation for such nearly periodic X-ray variability in most AGNs might be that the flux arises from hot spots, spiral shocks, or other nonaxisymmetric phenomena related to orbital motions very close to the innermost stable circular orbit around an SMBH (e.g., Zhang & Bao 1991; Chakrabarti & Wiita 1993; Mangalam & Wiita 1993). In the case of AO 0235+164, a 17 day period at the inner edge of a disk corresponds to an SMBH mass of $1.7 \times 10^9 M_\odot$ for a nonrotating BH and $1.1 \times 10^{10} M_\odot$ for a maximally rotating BH (e.g., Gupta et al. 2009). While the latter mass is quite high, the former is a reasonable value, so it is conceivable that a temporary hot spot in the inner region of an accretion disk is somehow responsible for the observed quasi-periodic variations. However, for 2321+419 a 420 day period yields an SMBH mass of $7.5 \times 10^{10} M_\odot$ for a nonrotating BH and $4.8 \times 10^{11} M_\odot$ for a maximally rotating BH. In this case, in order to reduce the SMBH mass to a quite high, but conceivable, value of $3 \times 10^9 M_\odot$, in either case of BH spin the dominant hot spot would need to be located at a distance of ~51 Gpc$^{-2}$ from the SMBH, which seems to be rather far away for a hot spot that contributes significant flux. Another reason to discount this hot spot scenario for both blazars is that blazar disks are almost certainly close to face-on but large hot spot amplification arises from near-field gravitational lensing and that is strong only if the observer’s line of sight is close to the disk plane (e.g., Bao et al. 1996).

A somewhat related possibility is that we are seeing the interaction between a second BH and the disk surrounding the primary one, as seems to be the case for OJ 287 (e.g., Valtonen et al. 2008). However, such an orbital cycle should probably yield a more precise and long-lived periodicity than we have found for the X-ray emission of both AO 0235+164 and 2321+419, so we believe this hypothesis is quite unlikely. In addition, for AO 0235+164 the rather short period strongly disfavors the binary BH hypothesis.

The microlensing hypothesis does not appear to be able to produce a quasi-periodic component to the variability, so even if it does play a role in producing some variability in the observed flux of AO 0235+164, it is probably irrelevant to the fluctuations of interest here.

### 4.3. More Likely Explanations

As the preponderance of other evidence has the X-rays seen from blazars, particularly in active phases, emerge from their jets, and not their putative accretion disks or coronae, it makes sense to examine how such quasi periods could be related to jet structures. Turbulence behind a shock propagating down a jet (e.g., Marscher et al. 1992) is a very logical, but not yet carefully treated, way to produce variability. For such turbulent flows the dominant eddies’ turnover times should yield short-lived, quasi-periodic, but probably modest, fluctuations in emissivity. Regions at different distances behind the shock will emit preferentially at different wavelengths. But because Doppler boosting can greatly amplify (roughly by a factor of $\delta^2$ to $\delta^3$, e.g., Blandford & Rees 1978) even weak intrinsic flux variations produced by small changes in the magnetic field strength or relativistic electron density can be raised to the level at which they can be detected (e.g., Qian et al. 1991). This same Doppler boosting reduces the timescale at which these fluctuations are observed by a factor of $\delta$ compared with the timescale they possess in the emission frame. Although it is difficult to quantify these effects precisely, this mechanism does seem to provide an excellent way to understand the optical intranight variability with quasi periods of tens of minutes that are only occasionally seen and that have timescales that vary from night to night in the blazar S5 0716+714 (Gupta et al. 2009).

The same turbulence in shocked-jet scenario could be playing out in a blazar such as AO 0235+164, where the fairly high value of $\delta \approx 10$ easily allows for modest fluctuations to become easily visible; however, the observed period of ~17 days converts into an eddy turnover time of ~87 days in the rest frame for such a Doppler factor. This would require a much larger, but still reasonably sized, eddy to be involved.

For 2321+419, this turbulent jet explanation is somewhat less likely to work if the Doppler factor is only ~1.7, as it would only produce amplifications of 5 or less. Moreover, the nominal rest-frame eddy turnover time would be ~675 days, which implies quite a substantial sized eddy and that the X-ray variations were arising at distances >1 pc from the nucleus.

It is quite likely that blazar jets will possess some essentially helical structure, such as can easily be induced by
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Camenzind, M., & Kroekenberger, 1992; Gopal-Krishna & Wiita
1992). There is no reason why the intersection of a relativistic
shock with a quasi-helical perturbation would not perform similar
feats for the X-ray emission, even though these high-energy
photons are unlikely to emerge from exactly the same jet regions
as the optical and radio photons (e.g., Marscher et al. 2008) and
should have somewhat different temporal dependences.

Because of the apparently large Doppler factor of the jet of
AO 0235+164, the observed substantial and nearly periodic
components in its X-ray light curve can naturally be attributed
to the intersections of a relativistic shock with successive twists
of a nonaxisymmetric jet structure. The apparently modest
Doppler factor of the jet in 2321+419 makes this explanation less
immediately attractive; however, all other hypotheses work even
less well for this source if the estimated low-Doppler factor is
correct. So, the intersection of a shock with a nonaxisymmetric
jet structure also seems to be the most plausible explanation for
the behavior of this blazar.

5. CONCLUSIONS

We searched the RXTE/ASM light curves extending over 12
yr of 24 blazars for possible periodic variations using SFs. Many
of them showed apparent periods, but the majority of these were
close to 1 yr and presumably not real. The four blazars that
showed indications of nonartifactual periods were examined
further using DCFs and LSPs.

Two blazars showed nearly common periodic components to
their X-ray variability through all three methods and had low-
(less than 0.03) false alarm probabilities according to the LSP
method: AO 0235+164 shows an observed period of ~17 days
while 1ES 2321+419 has one of ~420 days.

It is quite unlikely that these nearly periodic fluctuations are
caused by orbiting hot spots on or above accretion disks or by
a companion BH crashing through an accretion disk on each
orbit. It is even less likely that these fluctuations are produced
by microlensing.

Turbulence behind a shock moving through a relativistic
jet may provide an adequate explanation of our results if the
variations are dominated by large-scale eddies moving into and
out from our line of sight. Still, the most attractive hypothesis
to explain these variations appears to be the intersection of
a shock with an essentially helical structure wrapping around
the relativistic jet. In this case, X-ray polarimetry variations
should be correlated with the flux changes (e.g., Gopal-Krishna
& Wiita 1992) and might eventually provide a way to distinguish
between these different possible explanations.
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