THE AU MICROSCOPII DEBRIS DISK: MULTIWAVELENGTH IMAGING AND MODELING

Michael P. Fitzgerald,1,2 Paul G. Kalas,1,2 Gaspard Duchêne,3 Christophe Pinte,3 and James R. Graham1,2

Received 2006 November 15; accepted 2007 May 27

ABSTRACT

Debris disks around main-sequence stars are produced by the destruction of unseen parent bodies. AU Microscopii (GJ 803) is a compelling object to study in the context of disk evolution across different spectral types, as it is an M dwarf whose nearly edge-on disk may be directly compared to that of its A5 V sibling β Pic. We resolve the disk from 8–60 AU in the near-IR JHK′ bands at high resolution with the Keck II Telescope and adaptive optics, and develop a data reduction technique for the removal of the stellar point-spread function. We measure a blue color across the near-IR bands, and confirm the presence of substructure in the inner disk. Some of the structural features exhibit wavelength-dependent positions. Recent measurements of the scattered-light polarization indicate the presence of porous grains. The scattering properties of these porous grains have a strong effect on the inferred structure of the disk relative to the majority of previously modeled grain types. Complementing prior work, we use a Monte Carlo radiative transfer code to compare a relatively simple model of the distribution of porous grains to a broad data set, simultaneously fitting midplane surface brightness profiles and the spectral energy distribution. Our model confirms that the large-scale architecture of the disk is consistent with detailed models of steady state grain dynamics. A belt of parent bodies from 35–40 AU produces dust that is then swept outward by stellar wind and radiation. We infer the presence of very small grains in the region exterior to the belt, down to sizes of ~0.05 μm. These sizes are consistent with stellar mass-loss rates $\dot{M}_* \ll 10^{-2} M_\odot$.

Subject headings: circumstellar matter — instrumentation: adaptive optics — planetary systems: protoplanetary disks — stars: individual (AU Mic) — stars: low-mass, brown dwarfs — techniques: image processing

Online material: color figures

1. INTRODUCTION

In the past two decades, observations enabled by new technology have substantially broadened our understanding of dust surrounding main-sequence stars. These tenuous disks of dust, found around nearby stars, are fundamentally linked to the processes of star and planet formation (Backman & Paresce 1993; Lagrange et al. 2000; Zuckerman 2001; Meyer et al. 2007). Current scenarios favor casting “debris disks” in the later stages of the systems’ formation, after most of the primordial gas and dust have dissipated (on timescales of 1–10 Myr; e.g., Zuckerman et al. 1995; Haisch et al. 2001). The debris is freshly nourished by the sublimation, evaporation, and collisional destruction of orbiting parent bodies (for a recent review, see Meyer et al. 2007). Since a portion of these parent bodies may take part in the accretion of cores into planets—which may in turn gravitationally perturb the dust—circumstellar debris disks offer evidence for the presence of planets and insight into their formation.

Debris disks are usually discovered by sensing the thermal re-radiation of absorbed starlight in the far-IR (Backman & Paresce 1993; Decin et al. 2003; Bryden et al. 2006). The spectral energy distributions (SEDs) of these systems, particularly the range from the IR to the submillimeter, are commonly used to infer the (often cold) dust temperature and extent of disk inner clearing (e.g., Chen et al. 2005). However, in the absence of additional information, significant degeneracies exist in modeling the dust disks with SEDs (Moro-Martín et al. 2005 and references therein). Severe ambiguities between disk morphology and the grains’ physical characteristics are removed with spatially resolved images of the thermal and scattered light; however, the faintness of the dust and often large dynamic range between the star and disk present significant obstacles to their acquisition. Resolved images are both rare and valuable.

Images at multiple wavelengths are yet more powerful. Spatially resolving the debris across several wave bands provides definitive evidence for the size, space, and compositional distributions of the grains (e.g., Pantin et al. 1997; Wyatt 2006; Golimowski et al. 2006). Coupling such data with detailed models of grain dynamics can expose the fundamental physical phenomena governing the production and diffusion of dust throughout the disk. Physical models trace the characteristics of grains (i.e., composition and geometry) to the underlying parent body distribution, which in turn enables inferences regarding the coagulation history of solid material. These parent bodies may be corralled into a specific architecture through the gravity of nearby planets. Moreover, planets can imprint their signatures on the dust disk itself (e.g., Liou & Zook 1999; Wyatt et al. 1999; Ozmeyov et al. 2000; Kuchner & Holman 2003; Kenyon & Bromley 2004; Wyatt 2006). Tracing the mechanisms of grain dynamics through resolved imaging also addresses crucial questions about the nature of dust production in these systems—is the dust distribution steady state, or is the evolution of debris governed by transient events, such as rare collisions between massive bodies or extrasolar analogs to the late heavy bombardment? Again, the images that are critical to addressing these issues are rare, although the number of resolved systems has increased rapidly in the past few years (for recent tabulations, see Kalas et al. 2006 and Meyer et al. 2007). With ever-increasing sample sizes, we have entered an era..
where we can compare the structure and evolution of circumstellar dust with quantities that shape the paths of planet formation, such as stellar mass and metallicity.

Contemporary work has revealed an exciting laboratory for the detailed study of circumstellar debris. AU Microscopii (GJ 803) is a nearby star that harbors an optically thin debris disk. The spectral type in the literature ranges from dM0 to 2.5Ve (Joy & Abt 1974; Linsky et al. 1982; Keenan 1983; Gliese & Jahreiss 1995). It is a member of the Pictoris moving group, and as such is one of the youngest (12+3–4 Myr; Barrado y Navascués et al. 1999; Zuckerman et al. 2001) and among the closest (9.94 ± 0.13 pc; Perryman et al. 1997) of the known resolved debris disks. It is especially attractive to study in the larger context of disk evolution as a function of stellar mass. In terms of mass, M dwarfs like AU Mic constitute the dominant stellar component of the Galaxy. Despite the abundance of such stars, AU Mic is currently unique among the resolved debris systems. It is a touchstone for studying the evolution of circumstellar disks around low-mass stars. AU Mic has a well-chronicled history of flare activity (e.g., Robinson et al. 2001). It is likely that strong stellar activity has a significant effect on dust dynamics and lifetimes (Plavchan et al. 2005). Notably, we can make direct comparisons across spectral types given AU Mic and its sibling β Pictoris, the archetypal A star with an edge-on debris disk.

The scattered light of the dust around AU Mic was discovered by Kalas et al. (2004), who used seeing-limited R-band coronagraphic imaging to resolve it into an extended, near-edge-on disk. Additional high-resolution studies followed, with adaptive optics (AO) observations at H band by Liu (2004, hereafter L04) and Metchev et al. (2005, hereafter M05), as well as in the visible with the Hubble Space Telescope (HST) by Krist et al. (2005, hereafter K05). These detailed images reveal a very thin midplane (FWHM ~ 2 AU) with an inner disk closely aligned with the line of sight (θ ~ 0.5° for r < 50 AU; K05). The midplane surface brightness profiles show a break around 35–45 AU, with brightness decreasing more sharply at larger projected distances. There are slight asymmetries in the overall brightness of the profiles between the two disk ansae. Further, the midplane exhibits substructure on smaller scales, including localized enhancements and deficits in brightness, and vertical deviations of midplane positions away from that of a uniform disk. Comparison of these structures between data sets is required to confidently reject image processing artifacts. The origin of the small-scale structure remains unexplained. A striking feature of the scattered light disk is its color. K05 found a blue color in the visible with HST, along with an apparent color gradient—the disk is increasingly blue from 30–60 AU. The disk is also blue from the visible to the H band, as noted by M05. This is unlike many of the disks resolved to date, which are neutral or red scatterers like β Pic (Golimowski et al. 2006; Meyer et al. 2007). We note, however, that two other recently imaged disks, HD 32297 (Kalas 2005) and HD 15115 (Kalas et al. 2007), also scatter blue between the optical and near-IR. Such data are important because images at each new wavelength serve to further constrain the sizes, composition, and structure of grains through analysis of their scattering properties.

While the scattered-light imaging of the disk has attracted attention in the past few years, there has also been significant study of the grains’ thermal emission in the SED. The cold dust around AU Mic was first identified by the Infrared Astronomical Satellite (IRAS), as excess emission at 60 μm was weakly detected (Mathioudakis & Doyle 1991; Song et al. 2002). Recently, sensitive measurements of the 850 μm flux confirmed the presence of cold dust around the star (Liu et al. 2004). The Spitzer Space Telescope has further constrained the thermal emission of the dust in the mid-IR (Chen et al. 2005).

Results of these studies have been taken as indirect evidence for the presence of planets around the star. The gravitational influence of such planets provides a possible mechanism for generating the substructure in the disk. In particular, mean-motion resonances from a planet can trap dust to produce radial, azimuthal, and vertical structure (e.g., Oziernoy et al. 2000; Wahhaj et al. 2003; Thommes & Lissauer 2003; Wyatt 2006), although to date, no models of these mechanisms have been applied to the substructure of AU Mic. Further, the shallow surface brightness profiles in the inner disk and lack of thermal excess in the 10–20 μm region of the SED have suggested an inner clearing of dust, perhaps maintained again by the presence of an inner planet (e.g., Roques et al. 1994; Moro-Martín & Malhotra 2005). Nonetheless, it is imperative to understand the detailed physics affecting the distribution of dust grains around this disk prior to establishing the presence of unseen planets. The gravity of such perturbers is just one of many effects which may shape the dust distribution, including grain–grain collisions, forces from both stellar radiation and wind, and gas drag. Because the disk is along the line of sight to the star, AU Mic is a favorable target for using absorption spectroscopy to search for remnant gas in the disk. Roberge et al. (2005) placed limits on the column of H2 toward the star using the Far Ultraviolet Spectroscopic Explorer (FUSE), concluding that giant planets were unlikely to have formed given the rapid dissipation of primordial gas. Different groups have placed planet detection limits around the star in very narrow (r < 2″ ≈ 20 AU; Macciard et al. 2005) and slightly wider fields (Neuhäuser et al. 2003; M05), and to date none have been directly detected. Certainly the question of planets in this system warrants further study, as these different lines of evidence have not been resolved.

Comprehending the physics that sculpt the dust distribution in this debris disk remains a key step for not only determining the existence of planets, but also for informing us about the evolution of solid material around stars in general. Augereau & Beust (2006) and Strubbe & Chiang (2006, hereafter SC06) have both investigated the observed break in the midplane surface brightness profile and color gradient in the outer disk, and hypothesize that a ring of parent bodies (near the break in surface brightness profile) acts as a source of dust grains, which are subsequently swept outward by a strong stellar wind. SC06 provide a detailed physical model for AU Mic for this scenario. The steady state spatial and size distributions of dust grains are determined by a small set of physical processes (e.g., collisions, radiation, wind, etc.), and with other assumptions about grain properties, the model can reproduce observations of scattered light profiles and the SED.

As illustrated by the work done to date, we have constraints on the distribution of dust using scattered light images coupled with the SED. However, in this edge-on system, a degeneracy remains between the scattering properties of grains and their supposed spatial distribution. The advantage of measurements in polarized light, rather than total intensity, is that they give complementary information in the grain scattering properties (for grain sizes a such that a ≈ 2πaλ/C ~ 0.1) and thus reduce this degeneracy. The polarization properties of AU Mic’s disk have recently been measured with HST ACS by Graham et al. (2007). The disk exhibits strong gradients in linear polarization, and their modeling of the flux of polarized visible light indicates the presence of small porous grains and an architecture consistent with a significant (>300:1 in vertical optical depth to scattering) inner clearing.
In this paper we report and analyze multiband AO observations of the scattered light disk of AU Mic in the near-IR. Our high-contrast images were processed with a novel data reduction technique that aims to mitigate the effects of point-spread function variability on ground-based observations. We report on the observed colors and color gradients of the disk brightness profiles for our images, and also for reprocessed HST data previously presented by K05. Guided by the recent characterization of grain scattering properties by Graham et al. (2007) we simultaneously fit a dust model to near-IR and visible scattered light data as well as the SED. With this model of dust distribution, we then check the consistency of SC06’s physical model for the disk architecture with our empirical results. We examine the question of whether the inner disk is populated, as expected if corpuscular drag forces can draw grains inward before they are pulverized through collisions. We document our observational and data reduction techniques in § 2; we present our observational results in § 3 and analyze dust models in § 4. Discussion and conclusions follow in § 5.

2. OBSERVATIONS AND REDUCTION

The achievable spatial resolution is a prime motivator for imaging debris disks in the optical and near-infrared—resolved images here highlight structural details and dust properties. However, at these wavelengths the star overwhelms the light scattered by the circumstellar debris. This contrast ratio characterizes a fundamental observational challenge in such studies of debris systems. To meet this challenge, we use AO to concentrate the star’s light and employ a coronagraph to occult the resulting stellar image, thereby increasing sensitivity to the disk. Here, we detail our use of AO coronagraphy and image processing techniques to study the circumstellar dust (§§ 2.1–2.2). We describe calibration of the AO data in § 2.3, and our use of HST images in § 2.4.

2.1. Near-Infrared Imaging

We observed AU Mic on the nights of 2004 August 29–30 with the Keck II AO system and a coronagraphic imaging mode of the NIRC2 camera. AU Mic is sufficiently bright to serve as its own reference for adaptive wave front correction. After wave front compensation, the on-axis starlight is blocked by a focal-plane mask. Diffraction effects are then suppressed by a pupil-plane Lyot stop, and the light is reimaged onto a 1024 × 1024 pixel Aladdin detector. The narrow-field mode of the camera was used, at a scale of ≈10 mas pixel$^{-1}$. Exposure times were 30–60 s in $JHK'$ (60 × 1 s in $L'$), and the filter was cycled after a few short exposures in each band. Exposures where the disk was aligned with a diffraction spike were discarded. The filters, total integration times, and focal masks are listed in Table 1. We used a 0.5″ radius focal plane mask on the second night; however, the data in the region around the edge of this mask were discarded due to large residual subtraction errors. Calibration employed standard bias subtraction and flat-fielding techniques.

Imaging faint circumstellar material requires suppression of the stellar light, whose distribution is given by the on-axis point-spread function (PSF). While the coronagraph suppresses much of the starlight, a fraction leaks through the system and must be subtracted from the data in postprocessing. The relative success of this operation is linked to PSF stability. In observations through an altitude-azimuth telescope like Keck, the image plane rotates relative to the telescope with parallactic angle. However, features in the PSF that are produced by the telescope (e.g., diffraction spikes) maintain a fixed orientation relative to it. We disabled the instrument rotator of NIRC2 to additionally fix the orientation of any features arising from camera aberrations. With the disabled rotator, the PSF orientation is fixed relative to the detector while the edge-on disk appears to rotate around the stellar image with time. This allows us to disentangle the image of the disk from features in the diffraction pattern of the star, as well as use the stable orientation of the stellar PSF on the detector for more accurate subtraction. “Roll subtraction” is a general observational methodology that has been applied with success to AO imaging of circumstellar disks (e.g., L04, M05). An account of our version of the roll subtraction technique follows.

2.2. PSF Subtraction Technique

The time variability of the AO PSF is often the limiting factor in detecting faint circumstellar material from the ground. Rather than subtracting the stellar PSF from noncontemporaneous observations of reference stars, we wish to directly exploit information from the science target exposures. Techniques developed by Vérany et al. (1997) and Sheehy et al. (2006) seek to model the AO system to estimate the PSF, using telemetry data and crowded field imaging, respectively. However, these techniques do not yet have demonstrated applicability to high-contrast imaging. For roll subtraction, mitigation of AO PSF variability can potentially improve contrast. We note in particular the technique’s advancement in this regard by Marois et al. (2006) for the case of point-source detection.

We developed an algorithm suited to the self-subtraction of time-varying AO PSFs and applied it to the reduction of our near-IR images. In essence, because the PSF remains in a fixed orientation while the edge-on disk rotates, one may use PSF information spanning several exposures to estimate the stellar PSF (effectively removing the disk). Our refinement to the procedure is to estimate the PSF for each exposure, rather than for the ensemble. The PSF estimates are then used to subtract the stellar image from each frame. The residuals are transformed to a common sky orientation and then combined to estimate the star-subtracted object field (Fig. 1), corresponding to the disk emission. We detail our procedure, including the refinements for tracking changes in the time-variable AO PSF, in Appendix A.

2.3. Calibration

Immediately after bias subtraction and flat-fielding, we corrected the camera’s geometric distortion in each image. However, no attempt was made to calibrate for the scale and orientation of the detector on the sky, as any differences from nominal values are expected to be minor. When visually comparing with HST imaging (§ 2.4), we found a 0.1° rotation between the two sets.

| Night          | Band | $r_{\text{mask}}$ (arcsec) | $T$ (s) | $\Delta$P.A. (deg) |
|----------------|------|----------------------------|--------|-------------------|
| 2004 Aug 29....| $J$  | 0.75                       | 600    | 16.9              |
|                | $H$  | 0.75                       | 690    | 49.8              |
|                | $K'$ | 0.75                       | 1110   | 40.5              |
| 2004 Aug 30....| $J$  | 0.50                       | 570    | 39.0              |
|                | $H$  | 0.50                       | 600    | 34.5              |
|                | $K'$ | 0.50                       | 1260   | 45.6              |
|                | $L'$ | 0.50                       | 720    | 43.6              |

Notes.—The radius of the coronagraphic focal plane mask is given by $r_{\text{mask}}$. Filters were cycled after a few short exposures in each band. Here, $T$ is the total integration time and $\Delta$P.A. is the total amount of field rotation over the course of the exposure sequence in that band.
Our calibrations for photometry require measurement of zero point and PSF. We bracketed our observations of AU Mic with photometric standard stars SJ 9170 and HD 205772 on the first night, and GJ 811.1 on the second (Elias et al. 1982; Persson et al. 1998). These observations were used to determine the photometric zero point in each band. The stars were positioned outside the coronagraphic spot, and aperture photometry was used to measure the stellar brightness. Since large aperture radii could be used on the well-exposed stellar images, no encircled energy corrections were used in determining zero points. For all measurements, we applied an air mass correction assuming extinction values appropriate for Mauna Kea (Krisciunas et al. 1987).

To measure the scattering properties of the dust, we express the disk flux relative to that of the star. However, measuring the brightness of AU Mic is a challenge with this instrumental configuration because it is too bright for direct unocculted imaging, while observations using the focal plane mask complicate calibration. Here we adopt 2MASS photometry for the stellar brightness ($J = 5.436 \pm 0.017$, $H = 4.831 \pm 0.016$, $K = 4.529 \pm 0.020$; Skrutskie et al. 2006). We ignore the small (~few centimagnitudes) color correction when transforming from $K$ to $K'$, as we expect disk photometry to be dominated by other errors. To determine the brightness of the star in $L'$, we first measured the brightness of GJ 811.1 through the partially transmissive focal plane spot in $L$. We then applied a color correction to compute the zero point (behind the spot) in $L'$, and measured the brightness of the AU Mic using the same photometric aperture, finding $4.38 \pm 0.04$ mag in $L'$. We note that our attempts to express the relative disk and stellar flux ratio should take AU Mic’s variability into consideration. The star regularly flares in the X-ray and EUV regions of the spectrum (for a review with application to grain dynamics, see Augereau & Beust 2006). Periodic variations in the visible regions of the spectrum, thought to be caused by spots ($\Delta m_{r} \sim 0.35$ mag, $P = 4.865$ days; Torres & Ferraz Mello 1973; Cutispoto et al. 2003), are also relevant. However, as noted by M05, for AU Mic these are likely not problematic since the contrast between spots and the photosphere is lower in the near-IR.

It is convenient to measure surface brightness in rectangular photometric apertures, as are used in the calculations detailed in § 3.2. Because of the difficulty in using coronographic observations to infer the off-axis (unobscured) PSF, we apply an aperture correction based on the enclosed energy in this aperture by using the unobscured observations of photometric standard stars as PSF references. In each band, we average the enclosed energy over azimuthal rotation of the reference PSF to simulate the final roll-subtracted image’s PSF. The aperture corrections we derived from these enclosed energy measurements are susceptible to variability in the AO PSF because the reference PSFs are measured noncontemporaneously from those of AU Mic. To estimate the systematic errors in the overall flux levels, we examined the random error in the enclosed energy of the reference PSF exposures in each band. The largest fluctuation on a single night was 16%. Although the combination of data from both nights will reduce this uncertainty ($\leq 11\%$), the potential for unmeasured changes in the PSF from the reference star to science measurements remains.

With caution in mind, we estimate the uncertainty in flux calibration error in the final near-IR images at 20% and note that, in general, unsensed fluctuations will tend to affect the shorter wavelength observations to a greater degree. This systematic calibration uncertainty will affect the absolute levels of the surface brightness profiles we measure in § 3.2, and depending on the degree in correlation between errors in calibration in different bands, the disk colors (§ 3.3). Measurements of color gradients will not be affected by this type of error.
2.4. HST Imaging

In order to compare disk images over a wider range of wavelengths, we reduced and analyzed data previously obtained with the Hubble Space Telescope Advanced Camera for Surveys in the F606W filter ($\lambda_c = 606$ nm, $\Delta \lambda = 234$ nm) on 2004 April 3; K05. We acquired the flat-field images of AU Mic and the PSF reference star HD 216149 from the HST OPUS pipeline. These data were further calibrated by dividing by an appropriate spot-flat and multiplying by a pixel area map. A final image of AU Mic was constructed by averaging three frames of 750 s integration each, with appropriate filtering to reject cosmic rays. The final image of HD 216149 was constructed by averaging eight frames of 225 s each. We subtracted the PSF subtraction in a manner described by K05. There was no need to apply our specialized roll subtraction technique (Appendix A) to these data because of the stability of the ACS PSF. The PSF-subtracted AU Mic image was then corrected for geometric distortion using a custom IDL routine (J. Krist 2006, private communication). We used the Tiny Tim PSF model5 (Krist & Hook 2004) to compute the enclosed energy in rectangular apertures to enable comparison of surface brightness profiles with our near-IR data.

We used the same method for computing midplane surface brightness profiles described previously (§ 2.3). We checked the consistency of our F606W midplane surface brightness measurements against those reported in K05’s Figure 4 (using their $0.25'' \times 0.25''$ apertures) and found that our measurements of the same data were uniformly $0.20 \pm 0.05$ mag brighter. The discrepancy is due to the fact that K05 divided their images by a factor of 1.124 when correcting their pixel areas from $28 \times 25$ mas pixel$^{-1}$ to $25 \times 25$ mas pixel$^{-1}$ (J. Krist 2006, private communication). However, the photometric calibrations, both in the image headers and produced by SYNPHOT, assume that the final undistorted image is processed using DRIZZLE. The drizzled data product is similar to the manual calibration performed above and in K05, except that it does not include a uniform scaling of the image by a factor of 1.124. To correct the error, the disk brightness values reported in K05 should be increased by this factor. We adopted K05’s value of $8.63 \pm 0.03$ mag for the stellar brightness.

Aperture size aside, our measurement methodology of the F606W midplane surface brightness profile presented in § 3.2 produces results consistent with K05 after scaling their surface brightness by a factor of 1.124. The stability of the HST/ACS PSF ensures that the flux calibration uncertainty, set by the 0.03 mag uncertainty in stellar brightness, is much lower than those of the near-IR bands. The stellar brightness in F606W was measured in unocculted images at the same epoch, so our measurements are unaffected by the star’s variability.

3. RESULTS

3.1. Disk Morphology

The PSF-subtracted images are shown in Figures 2 and 3. As observed by other authors, the disk has a near-edge-on morphology. The data in each band of Figures 2 and 3 has been divided by the corresponding stellar brightness, such that the resulting colors trace the relative scattering efficiencies of the dust. We find the disk decreases in brightness relative to the star with increasing wavelength, up to $K$-band, indicating an overall blue color. We do not detect the disk with strong confidence in $L'$.

The disk midplane shows vertical structure (Fig. 4). We fit a Gaussian function to the vertical profile of the disk as a function of projected distance. We subtract this profile from the image, scale the residuals by a smooth fit to the amplitudes of the Gaussians, and display the results in the left panels of the figure. This procedure clearly reveals the location of a sharp midplane. Broader features also show variation—the width of the best-fit Gaussians is not constant with projected distance from the star. This effect has been noted and studied by other authors (K05; Graham et al. 2007). Capturing the vertical structure of the disk is important for detailed physical models of the system. However, here and in § 4, we restrict ourselves to considering only the most basic disk properties and defer detailed two-dimensional modeling for future work. We will discuss the disk substructure (brightness enhancements and deficits) in § 3.4.

3.2. Surface Brightness Profiles

Midplane surface brightness profiles are useful metrics of disk structure. These profiles average over the vertical extent of the observed scattered light image, which is naturally integrated along the line of sight. This facilitates comparison with scattered light models by reducing the brightness distribution to one dimension. We note that this convenient technique can fail to capture variation in the projected vertical extent of the disk, although we do follow the vertical centroid as a function of projected position. Prior to computing our profiles, we fit a spline to the vertical midplane position along each ansa. We used $0.1'' \times 0.5''$ photometric apertures centered on these positions in unsmoothed images to extract the photometry (Fig. 5). The width of this aperture is chosen to provide sufficient spatial resolution along the disk midplane, while the height is sufficient to capture several vertical FWHM of the inner disk. As reported by Graham et al. (2007) the apparent F606W disk thickness increases outward, reaching the 0.5'' aperture height at $\sim 60$ AU. Beyond this point, these photometric apertures do not perform a vertical average; rather, they sample the midplane brightness.

Our PSF-subtracted $L'$ data exhibit very low S/N structures along the disk plane in $L'$ at separations of $\sim 1''$ from the star, although these may result from PSF subtraction errors. In Figure 5 we show upper limits on the disk brightness in this band.

The uncertainties in Figure 5 represent the random measurement errors. At each radius, the contribution from residual speckle and background noise sources was estimated from the standard deviation of photometry in apertures placed in an annulus, excluding the locations near the disk. The photon noise from disk photometry is also factored into the random errors. The inner and outer edges of the profiles are set by the requirement that S/N $\geq 1$. To estimate the contribution of PSF subtraction to the systematic errors, at each radius we compared the mean values of the off-disk apertures (placed in an annulus) to the random error estimated from their standard deviation. These are generally less than one, suggesting that any bias in the profiles is smaller than the estimated random errors. Another possible mechanism for systematic error arises in the near-IR data because the PSF estimates are derived from the target exposures (§ 2.2 and Appendix A). If there is insufficient field rotation in the images, light from the inner disk may be subsumed in the PSF estimate, resulting in a self-subtraction of the disk. Nearly all of our data sets have $\Delta P.A. > 30''$ (Table 1), sufficient to exclude this as a source of significant error. However, the 2004 August 29 $J$-band data have $\Delta P.A. \approx 17''$, which corresponds to one disk midplane FWHM at $\sim 8.5$ AU. The 2004 August 30 data have much more field rotation, so the effect on the inner region of the composite $J$-band surface brightness profiles is likely to be small. Finally, the uncertainties in Figure 5 do not include potential errors due to flux calibration, which may be as large as 0.2 mag for the $JHK'$ bands.
We conclude that, relative to the random errors, the systematic errors are unlikely to affect the shape of the surface brightness profiles at separations greater than 8.5 AU.

By comparing our near-IR data to those of L04 and M05, we confirm a break in the overall midplane surface brightness profile around 30–35 AU. A break at /C24 15 AU in the F606W data was reported by K05, although the innermost points in our near-IR profiles are consistent with both a slight flattening and no break at all.

Broken power laws provide a compact description of the observed surface brightness profiles. Using flux-based units rather than magnitudes, we fit a function \( f(b) \propto b^{-\alpha} \) to the midplane surface brightness profiles in Figure 5, and report the resulting indices \( \alpha \) in Table 2. We scale the formal 1 \( \sigma \) random errors by \( \sqrt{\chi^2} \) when this quantity is >1 to partially account for the ill-fittedness of a strict power law to profiles that exhibit substructure. Errors in subtraction may be correlated because some PSF structures have significant radial extent. We ignore measurement covariance in the analysis, and thus potentially underestimate and the quoted errors. We chose to fit over two domains in projected separation: an inner region of 15.0–32 AU, and an outer region of 32–60.0 AU. The innermost boundary was chosen to mitigate possible biases from systematic errors. The outermost boundary is an upper limit, and is more precisely set by the availability of data in Figure 5. The break between the two regions was chosen to correspond to the kink in the midplane surface
brightness profile of the southeast ansa, corresponding to feature C (§ 3.4). The power-law fits of our H-band data are somewhat consistent with those of L04, who measures for the northwest (southeast) ansa $\alpha = 1.4 \pm 0.3 (1.0 \pm 0.3)$ over 20–35 AU and $4.4 \pm 0.3 (4.4 \pm 0.4)$ over 35–60 AU. Using the same method as used in Table 2 on these ranges (but different aperture sizes and positions), we obtain $1.6 \pm 0.2 (1.5 \pm 0.1)$ and $4.4 \pm 0.2 (3.4 \pm 0.2)$, respectively. The values we compute for the southeast slopes are steeper in the inner region, but shallower outside. Our measurements are consistent with those of M05 over similar domains. Those authors measure $\alpha = 1.2 \pm 0.3$ over 17–33 AU and $4.0 \pm 0.6$ over 33–60 AU. Using these ranges and averaging over ansae (but different aperture parameters) we obtain $1.4 \pm 0.2$ and $3.8 \pm 0.2$. We have significant differences in our F606W power-law indices relative to those of K05. The authors, using apertures that are 0.25” tall in the direction perpendicular to the midplane, calculate $\alpha = 1.8$ over the domain 15–43 AU, and $4.7$ in the region beyond 43 AU, both of which are somewhat steeper than our findings of $1.6 \pm 0.1$ and $4.1 \pm 0.2$ (measuring from 15–43 AU and 43–70 AU with our apertures). However, measuring with $0.1'' \times 0.25''$ apertures over the region 43–60 AU and averaging the fit indices over both ansae, we find $\alpha = 4.7$—consistent with K05. The differences in these comparisons serve to underscore the sensitivity of such power-law measurements to methodology. These differences may arise from PSF subtraction residuals, aperture sizes, aperture center locations, and the fit domain. Inferences between different data sets should be based on consistent power-law fits.

3.3. Disk Color Variation

The blue color, relative to the star, of the scattered light was first reported by K05. It becomes increasingly blue at larger radii (F435W − F814W = 0.2−0.5 mag from 30–60 AU). The disk also scatters blue when comparing visible data to the H-band measurements of L04 and M05. The blue color of the scattered light extends to our JHK’ observations. Figure 6 shows the color as a function of projected radial position along the disk midplane. The stellar contribution to the apparent disk color has been removed in order to highlight intrinsic grain scattering processes. Systematic uncertainties in calibration are not included, although as discussed in §§ 2.3–2.4, these are expected to be $\leq 0.3$ mag for $K' - H$ and $J - H$, and $\leq 0.2$ mag for F606W − H. In the inner disk ($\leq 35$ AU), the observed color gradient is consistent with a flat profile, while the outer disk is increasingly blue with stellocentric distance.

3.4. Disk Substructure

The AU Mic debris disk is known to exhibit nonuniformity in its midplane surface brightness distribution (L04, K05, M05). In order to remove global structure and highlight localized variations, we divided each brightness distribution by a smooth function in each band. We obtained weighted fits of spline functions to the northwest and southeast ansae’s midplane surface brightness profiles (§ 3.2) and averaged the results. The order and smoothness of the splines used to enhance the data have direct bearing on the spatial frequency content of the resulting map and may affect the observed positions and brightness of disk features. We used the curfit routine of FITPACK⁶ to fit a cubic spline to the data in Figure 5, with smoothness $s = m + (2m)^{1/2}$, where $m$ is the number of data points in the profile. Figure 7 shows an F606W image and a JHK’ color composite that have been processed in this manner. The annotations give the locations of substructural features (A−E). To allow for more quantitative comparison of disk features, in Figure 8 we show surface brightness profiles processed in the same manner. In order to highlight the structure of midplane brightness, these profiles are computed with $0.1'' \geq 0.1''$ apertures.

The imperfect removal of time-variable features in the PSF may introduce systematic errors that can masquerade as disk

⁶ See http://www.netlib.org/dierckx.
structures, underscoring the value of independent observations when identifying particular features. Liu (2004) identified several features of the disk substructure, which were also observed by K05 and M05. In independent observations such as these, any changes seen in the structures may be due to PSF subtraction artifacts. However, given that AU Mic exhibits brightness variability due to starspots, it is also possible that these spots differentially illuminate the disk such that the spatial distribution of disk brightness is also time-variable. We also note that differences in feature position and brightness from different authors may arise via analysis methodology. As we have done in Figures 7 and 8, it is desirable to highlight features by dividing the data by a function \( f(b) \), where \( b \) is the projected stellar separation. For example, L04 used \( f(b) = |b|^{-1} \) (see his Fig. 3) and M05 used \( f(b) = b^{-2} \) (their Fig. 3b). In contrast, K05 use a fourth-order polynomial fit to the surface brightness profile for \( f(b) \), while we use a spline fit (detailed above). These more complicated functions can better capture the overall brightness profile of the disk, which does not follow a single power law. On the other hand, they can suppress the appearance of the broadest features (e.g., feature D in the northwest ansa).

The application of the spline fit to the F606W- and JHK’-band data allows us to eliminate analysis methodology as a potential source of variation in feature brightness and position. While there are minor differences in the apparent characteristics of features between the near-IR bands, distinct differences in feature location arise when comparing those seen in visible to the near-IR.

Feature A, which is a brightness enhancement seen in both ansae, is \( \sim 1 \) AU further from the star in the visible (26 AU) compared to the near-IR (25 AU). There is also evidence for a change in the position of this feature in the near-IR; in particular, the \( J \)-band centroid is further out than in \( H \) or \( K' \) (see Fig. 8). Feature B is a brightness deficit in the southeast ansa that also exhibits a similar inward-moving centroid with increasing wavelength. Feature C is a southeast brightness enhancement, broader
than A, that shows a different position depending on the wave band. In J and H, the feature centroid is at \(~\sim 32\) AU, while it peaks closer to 33 AU in F606W and \(K'\). Feature D (37 AU) corresponds to a broad enhancement on the northwest ansa, a narrower dip in the southeast ansa brightness, and the location of the vertical displacement of the northwest midplane. The position of this feature is not significantly wavelength-dependent in these data. We confirm K05’s identification of a dip in midplane brightness inward of feature A, which we denote “E.” The locations of the other features seen in F606W agree with the positions given by K05. The \(H\)-band positions and characteristics of features A–D compare favorably to the results of L04. Together these strengthen the evidence for \(~\sim 1\) AU differences in the positions of features A–C. In contrast, M05 measures positions for A and B slightly closer to the star (by 2–3 AU); however, those data are of lower S/N and the differences may not be significant. A summary of these results is given in Table 3.

There are additional deviations in brightness that are detected in multiple bands. The broad enhancement at \(~\sim 46\) AU in the southeast noted by K05 is also detected in all the bands we consider. The feature seen in the F606W data, characterized by a peak enhancement at 15 AU and sharper drop at 12 AU, has corresponding characteristics in the near-IR bands. In \(HK'\), the peak is seen at 12–13 AU and the inner cutoff at 11–12 AU. The outer extent of this feature decreases gradually from \(~\sim 20\) AU in F606W to 17 AU in \(K'\). The peak enhancement in the southeast at \(~\sim 12\) AU in F606W also has corresponding enhancements at 12–13 AU in J and H; an examination of the \(K'\)-band surface brightness profile (Fig. 5) suggests the enhancement may also be present at \(~\sim 13\) AU in this band, but is not visible in Figures 7 and 8 due to the spline fitting process.

3.5. Point-Source Detection Sensitivity

We do not detect any pointlike sources in the disk midplane. We have developed a methodology for utilizing the artificial insertion of point sources into an image to measure the detection sensitivities in both the background and the disk midplane. We detail our technique in Appendix B, and present our sensitivity limits in Figure 9. We indicate the predicted brightnesses of model giant planets from Burrows et al. (1997) placing limits on the presence of young, massive companions. We note the caveat that at young ages, the emission from Jupiter-mass planets may...
be sensitive to initial conditions (e.g., Fortney et al. 2005; Marley et al. 2007).

4. ANALYSIS

Models of the grain size and space distributions that reproduce the scattered light and thermal emission probe the dynamical processes affecting the dust distribution. Previous models of the AU Mic disk have attempted to model the SED (Chen et al. 2005) and the scattered light profiles (e.g., K05). Metchev et al. (2005) Augereau & Beust (2006) and SC06 tackled the task of simultaneously fitting both. Using continuous power-law descriptions for the grains’ space and size distributions (submicron to millimeter sizes), M05 find they cannot simultaneously account for the scattered-light color, the SED, and the break in the surface brightness profiles at ~35 AU. As an alternative to power-law density distributions, Augereau & Beust (2006) obtained surface density models via scattered-light profile inversion. They tuned the size distribution to simultaneously fit the scattered light and SED. A distribution of silicate grains successfully matched the F606W-band profiles and SED, and in a separate fit, the H-band profiles and SED could be matched using a minimum grain size that is 10 times larger than the visible case. This discrepancy implies that size distributions that match the scattered light colors underestimate the amount of large grains responsible for the submillimeter emission. A different approach was taken by SC06, who modeled the dynamical structure of the debris disk to match the F606W scattered light and SED. For sufficiently large values of the stellar mass loss rate $M$, this model produces a blue color, with an outward blue gradient.

These previous efforts highlight two essential results. First, the blue color of the scattered light suggests small dust grains scattering in the Rayleigh regime, i.e., submicron particles. Second, the shallow slope of the long-wavelength SED is best fit with large grains of up to millimeter size (grains larger than this are weakly constrained). More recently, Graham et al. (2007) demonstrated that the linear polarization of the F606W scattered light requires porous grains. These data are important because the degeneracy between scattering asymmetry and spatial distribution can weaken inferences of debris disk structure based solely on measurements of total intensity. As the structure, size, and compositions of the grains determine the scattering properties, the assumption of compact grain types in previous work warrants reexamination.

Our goal is to find the simplest description of the grains and their distributions that is compatible with the variety of available observational data. In § 4.1 we describe the methods and structure of our models, the process used to fit the models to the observed scattered light and SED, and the properties of the resulting best-fit models. We then examine these results in the context of the dynamical model of SC06 for a steady state grain distribution produced by a ring of parent bodies (§ 4.2).

4.1. Dust Modeling

4.1.1. Monte Carlo Radiative Transfer

We model the debris disk around AU Mic using MCFOST, a Monte Carlo radiative transfer code that uses the Stokes formalism to treat the interaction between dust grains and photons to produce SEDs, scattered light images, and polarization maps. MCFOST is fully described in Pinte et al. (2006) and we summarize its main features here. Monochromatic photon packets are emitted by the star and propagated through the disk. The optical depth through which the photon travels before it interacts with a dust grain is randomly chosen from an $e^{-\tau}$ probability distribution. Scattered light and the thermal SED are computed separately. When monochromatic scattered light images and polarization

![Figure 8](image_url)

**Fig. 8.** Substructure in disk profiles. Surface brightness profiles computed with 0.1″ × 0.1″ apertures have been processed in the same manner as Fig. 7, by dividing each wavelength’s profile by a smooth spline function derived from an average of the northwest and southeast profiles from Fig. 5. Feature locations derived for the near-IR data are indicated by solid vertical lines (A–E), while dotted lines indicate the feature locations in F606W data by K05.

| Location (AU) | L04 | K05 | M05 | This Work |
|---------------|-----|-----|-----|-----------|
| A             | ↑   | ↑   | 25  | 26        | 22        | 25        |
| B             | ↓   | ↓   | 28.5 | 29        | 26        | 28        |
| C             | ↑   | ↑   | 31  | 33        | 32        | 32        |
| D             | ↓   | ↓   | 37  | 37        | 38        | 37        |
| E             | ↓   | ↓   | ... | 23        | ...       | 21        |

**Notes:** Features are marked in Fig. 7. Arrows denote localized enhancements (↑) and deficits (↓) of disk brightness. Feature locations in K05 are seen in F606W, while L04 and M05 are H band. Average feature locations in the near-IR data from this paper are in the final column, based on visual positions in Fig. 7 with uncertainties of approximately ±0.5 AU. We newly designate the close-in feature E here.
maps are produced, photons are only allowed to scatter off dust grains, with a loss of intensity corresponding to the absorption cross section of the grain. When the SED is computed, photons are either scattered or absorbed, depending on the local albedo; in the latter case, they are immediately reemitted at a longer wavelength selected on the basis of the local dust temperature. Once photons exit the computing volume, they are stored in “reception captors,” corresponding to specific inclinations. Maps at all inclinations are simultaneously created, but in this study we focused on the most edge-on captor, which includes inclinations ranging from 88.9 to 90°, believed to be appropriate for the inner disk of AU Mic.

To calculate the thermal equilibrium of dust grains, and therefore SEDs, the dust properties must be known throughout the electromagnetic spectrum, from the ultraviolet to the millimeter regime. It is not possible to describe the dust grains with a simple parameterization based on the albedo and the phase function asymmetry factor, for instance, unless these are known at all wavelengths. Rather, MCFOST relies on Mie theory (i.e., the grains are assumed to be spherical or essentially randomly oriented), so the knowledge of the dust optical indices (the complex index of refraction) at all wavelengths is sufficient. Grains with complicated structure, such as porous aggregates, are approximated by spheres with an effective optical index at each wavelength. Mie theory is used to calculate the scattering and absorption properties for these effective-medium spheres. In the case of AU Mic, small Rayleigh-scattering grains are indicated by the blue color and high polarization fraction (Graham et al. 2007). For composite grains, an effective medium approximation (depending on the constituent materials and method for computing the effective indices) can be reasonably accurate in the Rayleigh limit (Voshchinnikov & Mathis 1999).

MCFOST was first developed to model gas-rich, optically thick disks surrounding T Tauri stars. Several features have been added to efficiently and correctly treat the case of optically thin debris disks like AU Mic. The first modification was to increase the computational efficiency of treating optically thin material. Rather than expend effort computing the fates of all random photons, the majority of which will not scatter off grains in the optically thin disk, we enforce the first scattering of each photon packet to occur within the disk. The expected noninteracting photons are not randomly generated; instead we analytically account for the corresponding transmitted starlight. This ensures that all randomly generated stellar photons scatter at least once in the disk without energy loss. Second, in the absence of gas and given the low density of dust particles, the dust grains cannot be considered to be thermally equilibrated with one another. Rather, we compute a size-dependent temperature for the grains, each being in equilibrium with the surrounding radiation field. In the case of the AU Mic disk, this results in a significantly different shape of

![Fig. 9.—Point-source detection limits (5 $\sigma$). The solid curves are for sources outside of the disk, while the dashed curves give limits for sources residing in the disk midplane. In some places the midplane is more than a magnitude less sensitive. No point sources were detected along the disk. Horizontal lines indicate the predicted brightnesses for the model giant planets of Burrows et al. (1997) at ages of 10 and 30 Myr (AU Mic is 12.3 $\pm$ 1 Myr; Barrado y Navascues et al. 1999). Initial conditions play a large role in the luminosity evolution of young $\sim 1 M_J$ planets, and these “hot start” models represent brightness upper limits (e.g., Fortney et al. 2005; Marley et al. 2007).]
the SED in the mid-infrared due to large difference in temperature between grains of different size. Future high-resolution spectra in the 10 μm region may measure features that can constrain the composition and size distribution of grains (e.g., Li & Greenberg 1998; Chen et al. 2006).

4.1.2. Model Construction

Disk models frequently assume power-law descriptions for both the geometry of the disk and the grain size distribution. This is unlikely to reproduce all observed aspects of the disk, such as the complex small-scale structure seen in the scattered light (§ 3.1). It is nonetheless a valuable approach for constraining some of the main system parameters and testing simple hypotheses. Here, we attempt to reproduce the observations of the disk (SED and scattered light profiles) with a two-zone disk description. In a narrow inner zone, large grains would be present and account for most of the long-wavelength thermal emission, whereas a much more extended outer region would contain small grains and be responsible for the scattered light. This is a model that qualitatively matches models proposed by SC06 and Augereau & Beust (2006), where our inner annulus would represent the observable population of parent bodies and the outer zone the populations of small grains created by collisions of large bodies and swept out by pressure forces.

In both regions, we assume that the surface density and the grain size distributions follow Σ(r) ∝ r^p and dN(a) ∝ a^-μ da. The outer radius is fixed at 300 AU, as scattered light has been detected out to a sensitivity limit of 210 AU (Kalas et al. 2004). The inner radius and transition radius between the inner and outer regions are free parameters. In addition, the surface density index, minimum and maximum grain size and distribution index, and the total dust mass in each of the two zones are free. We initially use a γ = −7/2 index for the size distribution, which is commonly assumed for debris systems and is suitable for a steady state collisional cascade (Dohnanyi 1969). While both theory and observations may suggest specific functional forms for the vertical density profile of the disk, we cede to our preference for simplicity and assume that the vertical density distribution follows a Gaussian with a fixed width of σ = 0.8 AU and a flat radial dependence. In this case, the photometric apertures capture the majority of the scattered-light flux during brightness profile calculation. The particular choice of vertical density function is unimportant as long as the scale is much less than the photometric aperture height (§ 3.2). We defer for future modeling the exploration of relationships between the form of the vertical density profile, the dependence of scale height with radius, grain scattering phase functions, and the geometry of the disk.

The data for the SED were first compiled by M05 and supplemented with new Spitzer measurements by Chen et al. (2005). We use a T_⊙ = 3600 K, log g = 4.5 NextGen model for the stellar photosphere (Hauschildt et al. 1999), using radius R = 0.88 R_⊙ to match the observed stellar flux. For scattered light, we use the J-, H-, and K'-band profiles from data presented here, as well as the F606W-band profiles from data initially presented by K05 and reanalyzed for this work in § 3.2.

4.1.3. Fitting Procedure

Thorough exploration of the available parameter space is a time-consuming task when producing a SED and multiple scattered light images. We therefore explored it by hand, iteratively narrowing down the possible values for each parameter. Our objective is not to find the best possible model, but to determine if there is at least one solution based on this simple two-zone model that can match the data relatively well, which would in turn provide support to theoretical birth ring models (SC06; Augereau & Beust 2006). We compare our results to these models in § 4.2. To further reduce computation, we have elected to fit the F606W- and H-band profiles and the SED, and to later check for consistency with J- and K'-band profiles and F606W fractional polarization curves of Graham et al. (2007). We calculate the model profiles with the same rectangular aperture sizes as the observed profiles in § 3.2 (0.1'' × 0.5'').

We used a grain model that intrinsically includes a high porosity, a characteristic that provides both strong forward scattering and polarization—necessary features as demonstrated by Graham et al. (2007). The dust model developed by Mathis & Whiffen (1989) consists of a mixture of silicate, carbonaceous, and icy small elements combined into porous aggregates. With a_{min} = 5 nm, a_{max} = 0.9 μm, a size distribution index of γ = −3.9, and a vacuum fraction of 80%, this model reproduces the interstellar extinction law from the ultraviolet to the near-infrared. We used the same optical constants but allow the size distribution to vary. We fixed the inner zone’s size-distribution index to γ = −3.5. We searched for the power law distributions that would adequately produce the blue color (in terms of albedo × opacity) and roughly wavelength-independent phase function, so as to maintain roughly parallel surface brightness profiles from F606W to H. It was then possible to adjust the model parameters until a match to the SED and the scattered light profiles was obtained. We tuned the boundaries, grain size distributions, surface density indices, and total mass of each zone. For comparison, we also fit a model using the optical properties of compact silicate grains (from 2001) using the same procedure.

4.1.4. Fit Results

The parameters of our best-fit models are listed in Tables 4 and 5, and the results are shown in Figures 10 and 11. Considering the F606W- and H-band profiles and the SED, we obtain reasonable agreement with the predictions our two-zone model using porous grains: a region of large grains between 35–40 AU, and a region of smaller grains outward of 40 AU. These are slightly further out than the best-fit regions using compact grains, which are more isotropically scattering. We find that, if the particles in the inner region are porous, they must be in the millimeter regime (sizes of 3–6 mm). Allowing the size distribution to encompass smaller grains results in an overly steep long-wavelength SED, as well as a flux deficiency in the outer small grain region. Much larger bodies could be present yet undetectable; they would emit very little, even at millimeter wavelengths. For porous dust in the outer region, we require a distribution encompassing small grains (0.05–3.0 μm, dn ∝ a^{-4} da), with a power-law index that is steeper than the collisional steady state value of −3.5.

The masses in the inner and outer regions of the porous grain model are around 1.0 × 10^{-2} M_⊙ and 2.3 × 10^{-4} M_⊙, respectively. The surface density profile falls rapidly outside of the transition radius (index −2.5 to −3.0), as expected from swept up material; shallower indices yield an improved SED but insufficient scattered flux inside 40 AU and too-shallow profiles overall. Steeeper indices yield an excessively precipitous F606W-band brightness profile and excess flux around 50–100 μm. In the inner region, the surface density can be flat or increase with radius, peaking at the transition radius. This is only loosely constrained: the big grains never get very hot in this narrow annulus and there is little effect on the SED. We performed some exploration of the parameters to estimate uncertainties. The masses are relatively well constrained, to 50% or so, depending on the grain size distribution parameters. Again, more mass could be hidden in the form of very large bodies in the inner region; the mass derived here is just what is needed to reproduce
the long-wavelength end of the SED. In computing the total intensity of scattered light, there is an anticorrelation between $a_{\text{min}}$ and the region boundary at ~40 AU. We can adjust the minimum grain size by a factor of 2, and the ring radius by ±5 AU and still achieve satisfactory F606W- and H-band profiles and SED.

As demonstrated by Graham et al. (2007) the fractional linear polarization profiles provide a complementary constraint on the optical properties of the small grains. The measured fractional polarization gradually rises to a plateau of ~35% at around 50 AU. Our best-fit models using compact and porous grains are comparable in fit quality for the total scattered light intensity profiles and the SED; however, the polarization curves in Figure 11 clearly rule out compact grains, which reach maximum fractional polarizations <10%. The porous grains generally follow the measured trend, and reach a plateau of 30%–35% by 40 AU, the starting location of the small outer grain region.

This model has some shortcomings, in that it predicts excess flux around 60–70 μm and a slightly too-shallow scattered-light profile in the H band outside of the transition radius. This latter point results in a predicted disk color that does not change outside of 4.2, as opposed to the observations. We also note that the model profiles show less agreement with the K- and H-band profiles (Fig. 11). The overall flux levels differ (although this may coincide with photometric calibration uncertainty; see §2.3), and we overpredict the midplane surface brightness in the outer regions. For this analysis, we have avoided goodness-of-fit metrics like $\chi^2$ because our model, by design, will fail to reproduce substructure in the scattered-light profiles. Further, PSF subtraction residuals introduce correlations between errors in the measured profiles, which we ignore (§3.2). Nevertheless, we can get a sense of model fidelity by considering the long-wavelength end of the SED (where the dust contributes). For the nine SED points in Figure 10 at $\lambda > 10 \mu m$, the best-fit compact grain model gives $\chi = 8.6$ and the porous model gives $\chi = 10.9$. The bulk of the deviation arises from the 60–70 μm region. A formal $\chi^2$ analysis is not applicable, as we have also tuned our parameters to match the scattered light. In contrast to the porous grain model, the compact grain model underpredicts the 60–70 μm flux. With their higher average albedo, the compact grains absorb less energy than the porous ones (Table 5), suggesting a better fit may be obtained with grain albedos in the 0.6–0.7 range. Still, the fit is satisfying, considering the simplicity of the model (§4.1.2). Presumably, considering non–power-law prescriptions, other dust composition, non-spherical grains, and/or overlap between small and large grains would result in a better fit. One attractive possibility, that we do not explore here, is that ever-smaller grains are present as we move outside of the belt of parent bodies (§4.2). This could account for the increasingly blue color in the outer region as well as for the seemingly different transition radii obtained from the F606W- and H-band profiles (~40 vs. ~30 AU).

### 4.2. Birth Ring Examination

In the solar system, the asteroid belt and classical Kuiper belt constitute rings of solid bodies that, through mutual collisions, act as sites of continual dust production. Several forces act on the newly liberated grains, and the resulting trajectories shape the overall structure of the Sun’s debris disk. A similar belt of parent bodies has been invoked to explain the break in the surface brightness profile of the β Pic debris disk (Lecavelier Des Etangs et al. 1996; Augereau et al. 2001). Additional rings have been proposed to explain features seen in recent imaging (e.g., Wahhaj et al. 2003; Telesco et al. 2005) and spatially resolved spectroscopy (Weinberger et al. 2003; Okamoto et al. 2004) of this system. An attractive feature of such models is that their dust distributions are in steady state—we need not appeal to a rare (but recent) catastrophic collision between large (e.g., kilometer-sized) bodies, such that fresh grains have had insufficient time to completely diffuse through the system.

The breaks in the slopes of AU Mic’s surface brightness profiles naturally raise the prospect of a ring of parent bodies analogous...
to the classical Kuiper belt. The existence of such a belt was proposed by M05, SC06, and Augereau & Beust (2006). Here, we focus our attention on a detailed theoretical model, developed by SC06, which yields the steady state spatial and size distributions of dust grains in the disk. A critical parameter is the stellar mass-loss rate, \( \dot{M}_\star \), which governs the corpuscular forces on the grains. In addition to modifying the disk structure, the stellar wind is crucial in determining the lifetimes of debris disks around late-type stars (Plavchan et al. 2005). Assuming the scenario of steady state dust production by a ring of parent bodies is applicable, one may use a dynamical model to infer \( \dot{M}_\star \) from observations. We note that the theory was applied to the AU Mic disk prior to the observational findings of Graham et al. (2007), who showed that the disk’s scattered light is strongly polarized, and that porous grains are required to fit the polarization profile. In this paper we examine the disk structure predicted by the birth ring scenario in light of the currently available observational data. After a brief review of the predictions for compact grains, we probe modifications to the theory given the porous grains of our best-fit model and check the consistency of the theory’s features with those of our Monte Carlo radiative transfer model. In this context, we appraise the predictive power of the observations to determine \( \dot{M}_\star \) via inferences of the size and space distributions of grains.

4.2.1. The Theoretical Scenario

We first recapitulate the basic physical arguments of the model put forth by SC06. Collisions occur within the ring of parent bodies, producing dust grains. The radial components of forces arising from stellar radiation and wind result in a pressure acting to push grains away from the star, causing blow-out for sufficiently small grains. In contrast, the tangential components of these forces act as a drag mechanism, which for radiative forces is the well-known Poynting-Robertson (PR) drag. Grains dominated by drag forces spiral in toward the star. The competition between these forces and the relative frequency of destructive grain collisions determine the dynamical structure of the disk. In disks dominated by drag forces, (SC06’s “type A”), the action of PR and corpuscular drags fill the region interior to the birth ring.

Fig. 10.—Model fit to the scattered light and SED of the system. Left: The surface brightness profiles from Fig. 5 along with surface brightness profiles from the best-fit model. The gray boxes above the profiles represent the grain locations in our model (see Table 4); the dark region indicates the inner region of larger grains, while the smaller scatterers are in the lighter zone outside. Right: The model SED along with measured photometry of AU Mic. In this model, the smaller grains are responsible for the bulk of the scattered light and the mid-IR emission, while the larger grains reproduce the long-wavelength end of the SED.

Fig. 11.—Left: Comparison of the surface brightness profiles from Fig. 5 to surface brightness profiles from the best-fit model in J and K bands. These data were not used in the fitting process. The differences in overall flux may be due to photometric calibration uncertainties (\( \Delta I \)), although the model clearly overestimates the emission in the outer zone in these bands. More complicated models may resolve these discrepancies; a changing minimum grain size with radius can produce a color gradient. Right: The fraction of linear F606W polarization produced by our model compared to measurements of Graham et al. (2007), which include both systematic and random errors. Compact, micron-sized grains are ruled out by these data.
with grains that avoid destructive collisions. In disks dominated by collisions ("type B"), this interior is essentially empty, as the pulverized remains of colliding grains are quickly swept outward. In both cases, the region exterior to the birth ring is largely populated by the small, tenuously bound grains that follow elliptical orbits with periastra near the birth ring. In type-B disks, these grains are just larger than the blow-out size of stellar wind and radiation pressure. In type-A disks, the smallest grains are pulled inward by corpuscular and PR drag, and the peak of the grain size distribution in the outer disk corresponds to a size significantly larger than that of blow-out.

SC06 developed analytical and numerical descriptions of the results of these processes on the size-space distributions of dust grains, and then applied this theoretical framework to the case of AU Mic. They postulate a belt of parent bodies at 43 AU, a location determined by the surface brightness profile break in HST imaging. By simultaneously modeling the scattered light profiles (F606W-band from K05 and H-band from M05) and the SED with compact spheres of pure water ice, they determine that type-B conditions hold and place limits on $M_*$. With these assumptions on grain type, there are two pieces of evidence for an inner disk devoid of in-spiraling grains, which is expected for type-B conditions: (1) a lack of photospheric excess in the 10 $\mu$m region of the SED, and (2) the shallow slope of the surface brightness profile at projected distances interior to the proposed ring. Augereau & Beust (2006) argue for a similar dynamical scenario for explaining the observed structure, where corpuscular pressure forces sweep grains outward. Considering the pressure from the stellar wind (and additional radiative enhancement by stellar flares), they determine that radial forces can sufficiently diffuse small grains into the outer regions to account for the observed profile break, in analogy with the dominance of radiation pressure in β Pic's disk.

### 4.2.2. Potential Ramifications of Porous Grains

It is important to examine the birth ring scenario in view of the new constraints on scattering properties from recent imaging of the disk in polarized light (Graham et al. 2007). The polarization data strongly indicate the presence of porous grains scattering in the Rayleigh regime, reaffirming in our modeling (§ 4.1.4). Such grains are largely forward-scattering and produce the required high peak polarization fraction. Since scattering asymmetry directly affects the inferred spatial distribution of grains, previous models’ use of spheres of solid material must be reevaluated with this new evidence. We also stress that, as noted in § 3.2, analyses involving surface brightness profiles require consistent methodology across all data sets. Following these points, it is appropriate to both check the consistency of the model by SC06 with our porous grain Monte Carlo model, and to evaluate the strength of such models for inference of AU Mic’s stellar mass-loss rate.

In approaching this problem, it is apt to contrast the relevant properties of the compact and porous grain types we use in the models of § 4.1. As expected, the porous grains of Mathis & Whiffen (1989) are less dense than the compact grains, at $\rho = 0.5$ g cm$^{-3}$ (compared to 2 g cm$^{-3}$ for Draine & Li 2001 grains). At a given size, the porous grains also couple less efficiently to the radiation field than their compact counterparts. Taking a 0.05 $\mu$m grain as an example, the effective cross section for radiation pressure ($Q_{pr} \pi a^2$) is more than an order of magnitude smaller for a porous grain: $Q_{pr} \sim 2 \rightarrow 0.05$ when changing from compact to porous. This coupling inefficiency is similarly manifested in a decrease in the effective cross section to scattering, $Q_{sca} \pi a^2$, for porous grains.

Debris disk structure is commonly parameterized by the vertical optical depth. In the following analysis, we will refer to both the vertical optical depth to scattering, $\tau_{sca}$, and the geometric vertical optical depth, $\tau_{geo}$. The former quantity is useful for describing the one-dimensional brightness profile, while the latter governs the collisional timescale. For a given surface mass density $\Sigma$, the depth $\tau_{geo}$ depends only on the grain density and size distribution $dN/da$, while $\tau_{sca}$ additionally depends on scattering efficiency:

$$\tau_{geo}(r) \propto \int \frac{\pi a^2}{\rho} \frac{dN}{da} da,$$

$$\tau_{sca}(r) \propto \int \frac{Q_{sca}(a) \pi a^2}{\rho} \frac{dN}{da} da.$$  

For a given grain type and size distribution, $\tau_{geo}$ and $\tau_{sca}$ can differ by orders of magnitude. As an example, consider the outer region of porous grains in our model from the previous section. While the size distribution is steep ($dN/da \propto a^{-4.1}$), because $Q_{sca}(1 \mu$m $\gg Q_{geo}(0.05 \mu$m $\mu$m$)$, micron-sized grains constitute the bulk of $\tau_{sca}$ despite their relative scarcity. The geometric depth $\tau_{geo}$, on the other hand, is dominated by the smallest grains, resulting in $\tau_{geo} \gg \tau_{sca}$.

#### 4.2.3. Disk Structure Analysis: Theoretical Considerations

The models of SC06 delineate three regions of water ice grains: (1) a birth ring, populated by parent bodies of sizes up to ~10 cm, (2) an outer region made up of smaller grains ($a_{min} \leq 1 \mu$m) on loosely bound orbits, and in type-A disks, (3) an inner region of grains, $\leq 1 \mu$m size, spiraling inward as a result of corpuscular and PR drag forces. Grains smaller than the stellar wind and radiation pressure blow-out size, $a_{min} \sim 0.1 \mu$m, have negligible contribution to the disk. Our modeling of the dust distribution with porous grains (§ 4.1) shows that a two-zone architecture (lacking an inner region of drag-dominated grains) is consistent with the observations and, qualitatively, with the architecture predicted by physically modeling dust generated by a belt of parent bodies.

In the birth ring model, how does the expected grain size distribution change in light of the differences between the Mathis & Whiffen (1989) grains and water ice spheres? We first consider $a_{\text{blow}}$, which is determined by the combined action of radiation and stellar wind pressures. The density decrease of porous grains relative to spheres tends to increase $a_{\text{blow}}$. However, this effect is offset by the decrease in the effective cross section, parameterized by $Q_{pr}$ (a factor for 40 lower for $a = 0.05 \mu$m grains), resulting in a net decrease of porous grains’ blow-out size relative to their compact counterparts. Rewriting SC06’s Eqs. 7 and 8, the blow-out size assuming constant pressure is

$$a_{\text{blow}} = \frac{3}{8\pi} \frac{L_\star}{GM_{\odot} c^2} \left( Q_{pr} + Q_{wind} \frac{M_r v_{wind} c}{L_\star} \right).$$

We follow SC06 in adopting $v_{\text{wind}} = 450$ km s$^{-1}$ and $M_r = 2 \times 10^{-14} M_\odot$ yr$^{-1}$. We choose $L = 0.12 L_\odot$ and assume that the cross section to wind ($Q_{\text{wind}} \pi a^2$) is unchanged ($Q_{\text{wind}} = 1$) for the porous grains. Together these yield $a_{\text{blow}} = \{0.029, 0.047, 0.23, 2.1\}$ $\mu$m for $M_r = \{1, 10, 10^2, 10^3\} M_\odot$. The minimum grain size in the outer region of our disk model (0.05 $\mu$m) is larger than $a_{\text{blow}}$ for the weaker stellar winds, which suggests $M_r < 10^2 M_\odot$.

Next, we consider the implications of our porous grain model on the amount of disk infill (type A vs. B) predicted by the birth ring theory—a process regulated by the collision rate, which
depends on $\tau_{\text{geo}}$ (eq. [1]). In our model for the scattered light at $r_{\text{BR}} = 40$ AU, the smallest grains contribute the bulk of the total geometric cross section. The abundance of these grains increases $\tau_{\text{geo}}$ at the birth ring relative to the SC06 value by a factor of 10, to $\tau_{\text{geo}}(r_{\text{BR}}) = 4 \times 10^{-2}$. This shortens the timescale for destructive collisions of the average particle, assuming the specific collisional energy is unchanged. The collisional timescale is balanced by the drag-induced infall time at a grain size defined by $a_{\text{break}}$ (see SC06, eqs. [36] and [37]). Grains near this size constitute the bulk of $\tau_{\text{geo}}(r_{\text{BR}})$, and in equilibrium, grains of sizes $a_{\text{slow}} < a < a_{\text{break}}$ fill the interior ($r < r_{\text{BR}}$). Like the case of compact ice spheres, for porous grains we find that $a_{\text{break}}$ is the same order as $a_{\text{slow}}$: $a_{\text{break}} = \{1.005, 1.03, 1.08, 1.1\}a_{\text{slow}}$ for a peak geometric vertical optical depth at $r_{\text{BR}}$ and the same stellar wind values. In contrast to SC06’s results for the compact grain case, we find that $(a_{\text{break}} - a_{\text{slow}}) < a_{\text{slow}}$ for porous grains in all wind cases, including stronger values. The implication of this result is that no amount of corpuscular drag will produce a significant fraction of grains with orbits crossing the inner region, favoring a clear inner disk (type B).

4.2.4. Disk Structure Analysis: Observational Limits on Infill

As a complement to examining the birth ring scenario, we can, for the moment, set aside the final conclusion of the previous section and use our model from § 4.1 to test allowed small-grain infill. When using MCFOST to model the observed disk with porous grains, can we make a distinction between the conditions of types A and B? By definition, our two-zone model lacks grains inward of the putative birth ring, consistent with a collisionally dominated type-B disk. To test whether the system could be consistent with type A, we now consider adding a third region of grains. If a significant mass of small grains are present inward of $\sim 35$ AU (type A), then these warmer grains would increase dust emission in the 10–20 $\mu$m region of the SED and add to the scattered light of the system (Figs. 10 and 11). We note that, compared to more isotropically scattering spheres, the strong forward scattering of porous grains allows us to hide more mass in this region without strongly affecting the total intensity of scattered light. The smallest projected separations, where the added contribution from forward scattering would be maximal, are lost in the glare of the central star and are behind the occulting spot.

The additional zone of porous grains has a flat $\Sigma(r) \propto r^\alpha$ density profile and ranges from 15–35 AU. The inner cutoff corresponds to the estimate of the ice boundary by M05 (13–15 AU). As a general feature of the birth ring conditions modeled by SC06, the outer region’s grains have $a_{\text{min}} \sim a_{\text{break}} \sim a_{\text{slow}}$, therefore we model a single-sized population of $a = 0.05 \mu$m grains in this new inner region. The middle and outer regions’ dust distributions were fixed to the best-fit parameters (Table 4), and we adjusted the mass in the new inner region in ~0.5 dex steps until the scattered light profiles (including fractional polarization) or SED showed significant deviation. We found that the SED first showed noticeable deviation at $M = 10^{-5} M_{\odot}$; this is an upper limit to the mass of grains in this population allowed by the observations.

We can express this limit as either the geometric or scattering vertical optical depths relative to the peak depth in the birth ring, $\zeta \equiv \tau_{\text{geo}}(r < r_{\text{BR}})/\tau_{\text{geo}}(r_{\text{BR}})$. The geometric vertical optical depth is more closely related to the dynamical structure, while the scattering depth is traced by our imaging observables. As noted in § 4.2.2, these geometric and scattering optical depths can be quite different. We find $\tau_{\text{geo}}(r < r_{\text{BR}}) \geq 2.5 \times 10^{-2}$, giving $\zeta_{\text{geo}} \leq 0.6$. While our limit to $\zeta_{\text{geo}}$ is order unity, the strong decline in $\zeta_{\text{geo}}$ with grain size results in a more stringent limit to $\zeta_{\text{sca}}$ for 0.05 $\mu$m grain filling. An inner mass of $3 \times 10^{-5} M_{\odot}$, easily ruled out by our analysis, corresponds to $\zeta_{\text{sca}} \sim 1/400$. This is the same order as the limit of Graham et al. (2007), who determined $\zeta_{\text{sca}} \leq 1/300$ inward of 40 AU using a similar method (although without SED modeling).

While the limit for $\zeta_{\text{sca}}$ implies an inner disk relatively free of scattering grains, the relevant quantity for the dynamical structure of the disk is $\zeta_{\text{geo}}$. The weakness of our geometric optical depth ratio limit implies that we cannot yet determine type-A versus type-B dynamics or make inferences of $M$, by matching the expected disk structure to current scattered light and SED data. Rather, perhaps the strongest direct observational evidence for a type-A disk would come from resolved thermal emission from this zone.

4.2.5. Future Considerations

When considering more rigorous tests of birth ring theory, several enhancements can be made to our simple disk model. Faithful models must not rely on an artificial separation between the site of dust production (inner, large-grain region) and the small grains, as we have done in § 4.1. SC06 also predict different asymptotic power laws for the outer region’s geometric vertical optical depth in type-A and type-B disks (~2.5 and ~1.5, respectively). However, the corresponding asymptotes in scattered light profiles are not reached until distances of a few 100 AU, ruling out reliable comparisons with current data. Somewhat more challenging aspects of the theory are grain size distributions that do not follow power-law description (see Fig. 3 of SC06). The prediction of SC06 is an excess of grains above the Dohnanyi collisional cascade ($dn \propto a^{-7/2} da$) for sizes near $a_{\text{slow}}$. Incorporating a population of grains at this size, in addition to the power-law size distribution, is a possible avenue for future significance testing. Both SC06 and Augereau & Beust (2006) predict diminishing minimum grain size with increasing stellar distance (due to ever more tenuously bound grains as a result of stellar wind and radiation pressure), which can effectively model the observed blue color gradient in the outer region. Future scattered light modeling may incorporate a function $a_{\text{min}}(r)$ in the outer zone.

5. DISCUSSION AND CONCLUSIONS

Debris disks are a long-lived phase in the evolution of circumstellar material, and they provide indirect probes for the presence of planets and planetesimals. Resolved imaging is crucial for determining the structure and dynamical history of the dust. In our near-IR imaging, we measured the structure of the disk seen in scattered light. We confirmed the overall architecture of the disk seen in $H$ band by L04 and M05, and presented the first images seen in $J$ and $K^\prime$ (§ 3.1). We represented the global disk structure with a power-law description of the midplane surface brightness, and noted that discretion must be used when comparing between profiles measured in different manners (§ 3.2). Scattered light features on both large and small scales are largely consistent across the bands studied here. The colors we measured in the surface brightness profiles (§ 3.3) allow inferences of the scattering properties, which are determined by the composition, sizes, and structures of dust grains.

We used a model for the space and size distributions of the grains to reproduce these profiles and the SED (§ 4.1). The simple, two-zone description of power-law grain distributions cannot faithfully reproduce the observations with compact silicate grains. Rather, porous grains of dirty ice, whose presence is indicated by recent polarization measurements (Graham et al. 2007), have optical constants with which we can match such an architecture to the data with reasonable fidelity. The key degeneracy is between the scattering phase function and the density distribution.
Models of K05 and M05 place grains that exhibit moderate scattering asymmetry in the inner regions of the disk. The porous grains in the outer zone of our model, which are larger and more forward scattering than the compact grains used in previous efforts, fill in this region of scattered light. As such, our modeling does not require grains inward of 35 AU to reproduce the mid-plane surface brightness profiles. The inner zone (35–40 AU) of our model is made up of few-mm-sized grains, which reproduce the far-IR end of the SED. The outer zone grains of our model are smaller (0.05–3.0 μm) and produce the majority of the mid-IR emission and the scattered light.

The blue color of the scattered light disk is relatively rare among resolved systems (see Table 1 of Meyer et al. 2007). The succession of modeling efforts have shown that a significant population of submicron grains reproduces the disk’s blue scattered-light color, and that the presence of such grains is compatible with interpretations of the disk’s dynamical structure. As other authors have noted, stellar properties play a major role in the removal of submicron grains. As an M dwarf, AU Mic has a uniquely low radiation pressure relative to other stars with scattered-light debris disks. For sufficiently low values of $\dot{\epsilon}$, we find $\eta_{\text{slow}}$ is submicron and grains will scatter blue. While stellar properties can reasonably be used as a predictor for the presence of submicron grains in debris systems, grain properties can also affect the blow-out size. As we noted in § 4.2.2, the smallest of our porous grains have much smaller $Q_{\text{op}}$ relative to their compact counterparts of the same size. The blow-out sizes we calculate for porous grains are up to a factor of 8 smaller than those of compact grains (as computed by SC06). When blue scattered-light colors are detected around earlier type stars with stronger radiation pressure (e.g., HD 32297 and HD 15115; Kalas 2005; Kalas et al. 2007), inferences of submicron grains may constrain their porosity and composition (see also Artymowicz 1988; Grigorieva et al. 2007).

The study of debris disk evolution hinges on accurate measurements of stellar ages and dust masses. The total observed mass of the disk in our model ($10^{-2} M_\odot$) is dominated by the millimeter-sized grains in the inner zone. Note that this is a factor of a few times smaller than the mass we derive for compact grains ($2 \times 10^{-2} M_\odot$). Although the equilibrium temperatures for the two grain types differ, this is primarily an opacity effect (Voshchinnikov et al. 2006). The decrease in density increases the opacity, which in turn lowers the mass needed to match the submillimeter fluxes. Since these grains contribute little to the scattered light, we have no information about their porosity (and correspondingly whether any compaction has occurred). Therefore, in addition to the normal caveats about dust masses derived from submillimeter fluxes (e.g., insensitivity to larger bodies), derived debris disk masses are additionally uncertain by a factor of a few depending on the grain porosity. The same opacity caveat applies to the inferred sizes of the grains that dominate the sub-millimeter emission. In the inner region, our porous grains are a factor of three larger than the equivalent best-fit compact ones—the increased opacity means a larger size is needed to match a given temperature.

Nevertheless, we can compare our dust masses to those of other authors. Our estimate is similar to the mass estimated by a single-temperature fit to the long-wavelength SED by Liu et al. (2004), who found $1.1 \times 10^{-2} M_\odot$ of 40 K dust at 17 AU. M05 found a similar mass as Liu et al., for single-zone power-law distributions of size and density of ISM-like grains. Augereau & Beust (2006) calculate a mass of $7 \times 10^{-3} M_\odot$ by adjusting the grain size distribution in their scattered light model in order to match the long-wavelength SED. Finally, SC06 argue for parent body sizes up to 10 cm, the maximum size participating in a steady state collisional cascade. For their model’s size distribution, the mass of parent bodies is $\sim 10^{-2} M_\odot$. However, current observations are not sensitive to grains larger than a few mm, so the maximum observed mass in this model is significantly lower. For size distribution index $\gamma = -7/2$, the mass $M \propto a_{\text{min}}^{3/2}$, and the observable portion of SC06’s mass is a few times smaller than that of our work.

The interpretation of debris disk observations for inferring the presence of planets and the history of the grains rests on sound physical modeling of grain dynamics. The overall shape of the midplane surface brightness profile distribution is consistent with steady state dynamics arising from a ring of parent bodies (§ 4.2). With models of grain dynamics, we might constrain $M$ by examining the density of small grains in the inner disk ($\lesssim 35$ AU). We found that for the porous grains in our model, an inner region would be populated primarily by grains just above the blow-out size for a wide range of $M$. Further, the constraint of the presence of grains in an inner region is set by the mid-IR SED, and we can only say that the geometric vertical optical depth in this region is at most the same order as the peak depth in the birth ring, consistent with both drag- and collision-dominated (types A and B) disks. However, the presence of small (0.05 μm) grains in the outer region implies that the mass-loss rate is low enough such that these grains survive blow-out, i.e., $M_c < 10^{-2} M_\odot$.

The overall disk architecture inferred from these models has implications for the substructure seen in scattered light. In § 3.4 we compared our measurements of features A–E with the results of other authors, giving further evidence that they are not artifacts of stellar PSF subtraction. Additional brightness enhancements located 11–15 AU from the star have also been identified, although additional observations of the disk at small angles are needed to improve confidence. The appearance of such substructural features is determined by the grain distribution; since the bulk of the scattered light comes from small grains beyond $\sim 40$ AU, the features at projected distances inward of $40$ AU must arise from azimuthal perturbations in the dust distribution beyond this distance. Some of these features appear to exhibit a wavelength-dependent position. (We note the position of feature D, which is closest to $40$ AU, does not appear to do so.) While the overall position of a feature may be used to trace a perturbation in the density distribution in the outer disk, the wavelength dependence of the position may constrain additional spatial variation in the grain size distribution. In a similar vein, any vertical structure associated with a given feature (Fig. 4) can be tied to the vertical structure of the outer disk.

In summary, we

1. demonstrate a new roll subtraction technique that attempts to mitigate AO PSF variability (§ 2.2, Appendix A);
2. detect the AU Mic debris disk in $JHK'$-band imaging and place an upper limit on the L'-band brightness distribution (§ 3.1);
3. confirm the blue color of the disk and measured a blue color gradient outside of the transition radius (§ 2.3–2.4);
4. place detection limits on point sources in the disk midplane (§ 3.5) and document a technique for determining point-source detection sensitivity in the disk midplane (Appendix B);
5. verify the presence of substructure in the inner disk, and shown that some features exhibit slight variation in their positions with wavelength (§ 3.4);
6. demonstrate the applicability of a simple two-zone model that simultaneously fits the scattered light profiles and SED (§ 4.1);
7. find that compact silicate grains cannot be used in our simple model, while porous, icy aggregates of silicate and carbonaceous grains can reasonably account for the observed thermal and scattered light (§ 4.1);
8. determine that a two-zone model is consistent with steady state grain dynamics dominated by collisions (SC06 type B; § 4.2); 9. show that, by relying on models of the inner disk \( r \leq 35 \) AU structure, we cannot place strong limits on the geometric vertical optical depth of small \( (0.05 \mu m) \) porous grains interior to the birth ring and therefore cannot yet constrain \( M_s \) from this approach alone (§ 4.2); and 10. show that the blow-out size for porous grains is consistent with modeled grain size distribution for \( M_s \sim 10^2 M_J \) (§ 4.2).

The next modeling steps will seek to utilize all available imaging and SED data. We note in particular that measurements of scattering in polarized light provide strong, complementary constraints on the composition and distribution of dust in this system. Future work will incorporate fitting to scattered light images rather than surface brightness profiles, and will begin to probe the vertical structure of the disk while taking into account the effects of projection and blurring by the PSF. Finally, we emphasize that the global structure of the debris can be explained by steady state dust production and diffusion, and we need not invoke a planet to clear the inner region of dust. However, the mechanisms responsible for maintaining the structure of parent bodies in the birth ring as well as the dust substructure remain undetermined.

The authors wish to thank John Krist for enlightening the intricacies of HST ACS coronagraphic data calibration, as well as Eugene Chiang, Christian Marois, Peter Plavchan, and Linda Strubbe for insightful discussions. This work was supported in part by the NSF Science and Technology Center for Adaptive Optics, managed by the University of California at Santa Cruz under cooperative agreement AST 98-76783. This work utilized observations with the NASA/ESA Hubble Space Telescope obtained at the Space Telescope Science Institute (STScI), which is operated by the Association of Universities for Research in Astronomy. Support for Proposal number GO-10228 was provided by NASA through a grant from STScI under NASA contract NAS5-26555. Some of the data presented herein were obtained at the W. M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California, and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W. M. Keck Foundation. This publication makes use of data products from the Two Micron All Sky Survey, which is a joint project of the University of Massachusetts and the Infrared Processing and Analysis Center/California Institute of Technology, funded by the National Aeronautics and Space Administration and the National Science Foundation.

**Facilities:** HST (ACS), Keck:II (NIRC2)

**APPENDIX A**

**ROLL SUBTRACTION FOR AO**

A decisive arbiter of subtraction fidelity is the stability of the stellar PSF. We refined the roll subtraction process (Fig. 1) to simply accommodate the time variability of ground-based PSFs. In general, the long-exposure AO PSF is a nontrivial function of atmospheric turbulence fluctuations, filtration by closed-loop AO, and additional quasi-static wave front errors arising from the optics in the system (“static speckles”). With the PSF structure arising from these effects in mind, we built an empirical model of the PSF for each exposure, and then used these models to optimally subtract the stellar image. Our proposed deconstruction hinges on the removal of the radial profile from each image. It is much more challenging to remove the stellar profile from images with face-on disks. The procedure outlined here is most suited for imaging edge-on disks from the ground.

**A1. PSF MODEL**

The ideal model PSF will reproduce the response of the imaging system to the starlight that has been occulted by the coronagraph. For our subtraction problem, we are interested in estimating the structure of the stellar PSF’s outer regions—outside of any coronagraphic focal-plane mask. For the moment, we ignore the focal-plane mask and consider only the case of a monochromatic image of an on-axis star. We approximate the adaptively corrected long-exposure point-spread function \( S(x) \) as the convolution (\( \ast \)) between a “static” PSF and a blurring kernel encompassing the time-variable wave front errors (e.g., Veran et al. 1997),

\[
S(x) \approx S_c(x) \ast \Lambda(x).
\] (A1)

Here, \( \Lambda(x) \) is determined by the variable wave front errors of partially corrected atmospheric turbulence, which, depending on correction level, has a characteristic width \( \ll \lambda/r_0 \) (where \( r_0 \) is the Fried length), \( S_c(x) \) is the PSF that would arise solely from time-independent wave front errors. For a circular pupil of diameter \( D \) with no obscuration, \( S_c(x) \) is the diffraction-limited Airy pattern of characteristic width \( \sim \lambda/D \).

With good AO correction, the structure of the long-exposure PSF is characterized by a diffraction-limited core and a seeing-disk halo. Features like diffraction spikes and individual speckles also play an important role in the structure. To further motivate our model, we first decompose the static PSF into the sum of its Airy core \( (\theta < 1.22 \lambda/D) \) and all other static speckles \( (\theta > 1.22 \lambda/D) \),

\[
S_c(x) = S_{c,A}(x) + S_{c,sp}(x).
\] (A2)

Note that since the core is sharply peaked relative to the halo scale in the blurring kernel \( (\lambda/D \ll \lambda/r_0) \), \( S_{c,A}(x) \ast \Lambda(x) \) is approximately proportional to \( \Lambda(x) \) itself; the scale factor \( \alpha \) is related to the Strehl ratio. For computational simplicity, we treat the blurring effect of \( \Lambda(x) \) on \( S_{c,sp}(x) \) by a scalar factor \( \beta \), which also correlates with correction level—decreased blurring increases peak speckle intensity. Further approximating (A1), we have

\[
S(x) \sim \alpha \Lambda(x) + \beta S_{c,sp}(x).
\] (A3)
We have simplified the PSF from a convolution of static and atmospheric terms (eq. [A1]) to a linear combination (eq. [A3]), and we now seek to increase computational efficiency further. First, we note that with this linear combination, it is straightforward to generalize to wide-band imaging since \( \Lambda \) and \( S_{s,sp} \) can each be represented by a linear combination of quasi-monochromatic PSFs. Second, although not strictly true under real conditions, we further assume that the blurring is symmetric in azimuth (\( \phi \)). This leads us to isolate the azimuthally symmetric radial profile of each term in equation (A3). For an exposure \( i \), we estimate the image of the star as

\[
\hat{S}_i(\theta, \phi) = \rho_i(\theta) + \beta_i S'_{s,sp}(\theta, \phi),
\]

with \( S'_{s,sp}(x) \) given by \( S_{s,sp}(x) \) with the radial profile removed and subsumed into the profile term \( \rho(x) \).

We treat the coronagraphic focal mask in our model (eq. [A4]) simply. Prima facie, the circular mask’s suppression of the stellar image will be absorbed into \( \rho \). Errors in centering the star behind the mask will result in additional leakage of light outside the spot via diffraction (Lloyd & Sivaramakrishnan 2005), an effect we ignore. These misalignments manifest themselves as subtraction errors in the vicinity of the mask edge.

A key requirement for our model is the profile-removed speckle map, \( S'_{s,sp}(x) \). In practice, we use the target images themselves to construct \( S'_{s,sp}(x) \). We remove the radial profile from each image, mask out the region around the (rotating) edge-on disk, and combine the results to form the speckle map. We additionally mask the diffraction spikes from each image when estimating the radial profiles \( \rho_i \), because the spikes’ blurring (which we treat only by a scale factor \( \beta_i \)) can bias the profile estimates. In practice, we mask the disk with a 0.5\('\) wide strip, and the spikes with regions that are 1.6\('\) wide, tapering inward for \( \theta \leq 5\('\). With \( \rho_i(x) \) and \( S'_{s,sp}(x) \) in hand, the PSF model for each image is parameterized solely by \( \beta_i \), which scales the speckle map.

### A2. SUBTRACTION PROCEDURE

We subtract the model PSF \( \hat{S}_i \) from each image. The map scale parameter \( \beta_i \) and a registration offset are tuned to minimize subtraction residuals, which are rotated to a common frame and combined to form the image of the disk.

Special software masks are used in various stages of the subtraction process. Diffraction spikes and the edge-on disk were masked during calculation of the radial profile. The disk was also masked from individual frames before they were combined to form the speckle map. Diffraction spikes, the focal plane spot, and the disk were excluded from consideration during the least-squares optimization of the PSF model subtraction. Finally, diffraction spikes were masked from the subtraction residuals before they were combined to form the final disk image.

In summary, the sequence is to

1. register each frame to a fiducial position using stellar centroid estimates;
2. mask the diffraction spikes and the disk, then extract the radial profile about the fiducial point (\( \rho_i \));
3. remove the profile and combine the residuals from each image to obtain the speckle map (\( S'_{s,sp} \));
4. construct a PSF model for each image, using a scaled speckle map (\( \beta_i S'_{s,sp} \)) and the radial profile (\( \rho_i \));
5. use an optimization method to subtract PSF model from image, solving for stellar position and speckle map scale (\( \beta_i \));
6. repeat the process from step (1) using updated centroid estimates if not in final iteration;
7. mask diffraction spikes, rotate the subtraction residuals into the sky’s frame, and combine to form the disk image estimate.

We find that, for these data, three iterations of this process is enough for convergence to visually detectable levels.

### A3. TECHNIQUE COMPARISON

The subtraction procedure described in the previous sections is compared with similar implementations in Figure 12. In panel \( a \), we follow the steps we outlined above. In panel \( b \), we restrict the model fitting process so that the scale of the speckle map (\( \beta_i \)) is fixed and only offsets were optimized. Finally, in panel \( c \) we discard the PSF models altogether and fit the offset and scale of an average PSF. No spike

![Fig. 12.—Comparison of different methods of roll subtraction. Panel \( a \) shows the resulting image from the technique described in § 2.2. Panel \( b \) is the same as \( a \), except the scale of the speckle map is not optimized (Appendix A2). For comparison, panel \( c \) registers an average PSF to each image, rather than fitting a PSF model. Each of these images is 8" on a side. In panel \( d \), we show the annular rms (excluding the disk) of photometry in 0.1" × 0.5" apertures as a function of radius for subtractions shown in panels \( a-c \). At a radius of 2" , curve \( b \) is 0.56 mag more sensitive than \( c \), while \( a \) is 0.16 mag more sensitive than \( b \). The gain in contrast when subtracting the profile highlights the suitability of the technique for edge-on disks.](image-url)
or object masking were used when combining residual images in panel c. In panel d we display curves of annular rms (corresponding to the photometric errors shown in Fig. 5), excluding the regions near the disk. These curves show that fitting the speckle scale gives modest contrast gain (≤0.1 mag), while larger gains are obtained when removing the radial profile of the observations prior to combination (~0.5 mag).

**APPENDIX B**

**MIDPLANE DETECTION SENSITIVITY**

When quoting sensitivity limits for the detection of point sources around a star, it is common practice to measure the standard deviation of pixel values in concentric annuli, σ(ρ), and to set a scale to this curve with artificially inserted sources. In this case, σ represents a by-eye threshold. Here we wish to extend this methodology for the case of sources within the disk. To this end, we adopt a model for the sensitivity and solve for this model's parameters through visual detection of randomly inserted sources (both inside and outside of the disk) and maximum likelihood techniques.

We assume that the process of detecting a source can be characterized by zero-mean, normally distributed background noise fluctuations. In this case, the background can be characterized by σ, and the probability of detecting a source (denoting D = 1 for detection) of flux f is given by

\[ P(D = 1|f, \sigma) = \frac{1}{2 \sqrt{\pi}} \exp\left(-\frac{f^2}{2\sigma^2}\right). \]  

(B1)

which is the cumulative normal distribution function. Our task is to determine σ, which we can assume is proportional to σ(ρ) in regions devoid of disk light. Similarly, in the disk midplane, we expect an additional contribution to the background fluctuations from the disk light. For our ground-based observations, these fluctuations are dominated by speckle noise (including Strehl fluctuations) rather than photon statistics, and therefore the variance of this contribution is proportional to the square of the disk brightness, \(I^2\) (e.g., Aime & Soummer 2004; Fitzgerald & Graham 2006). We model the sensitivity in the midplane by

\[ \sigma^2(x, \mu, \xi) = \mu^2 \sigma^2(x) + \xi^2 I^2(x). \]  

(B2)

We fix \(\xi = 0\) to model the sensitivity in regions devoid of disk light. We measure σ(ρ) with a sigma-clipped sample standard deviation of pixels in concentric annuli, excluding regions of disk emission.

We randomly generated positions and fluxes for artificial sources to be inserted in each of our ground-based images. Two populations of sources were generated—one set randomly distributed along the disk midplane, and another in the off-disk region. The number of sources in each population was drawn from a Poisson distribution, and no blending of sources was allowed. Fluxes were drawn from a log-uniform distribution about \(\mu\), \(\xi\), and \(\sigma\), and to set a scale to this curve with artificially inserted sources. In this case, \(\sigma = \sigma(\rho)\).

With these data in hand, the problem reduces to finding the most likely model parameters (\(\mu, \xi\)) given the set of artificial source positions, fluxes, and detections \([x_i, f_i, D_i]\). Our sensitivity curves will use the model parameters that maximize the probability density \(p(\mu, \xi|x, f, D]\)). This quantity can be rewritten with Bayes’ theorem,

\[ \begin{align*}
\rho(\mu, \xi)|x, f, D) &\propto p(\mu, \xi)p(x, f, D)|\mu, \xi), \\
&= p(\mu, \xi) \prod_i P(D_i|x_i, f_i, \mu, \xi)|\rho(x_i, f_i), \\
& \propto p(\mu, \xi) \prod_i P(D_i|x_i, f_i, \mu, \xi). 
\end{align*} \]  

(B3)

The final step is valid since we are free to choose the position and flux distribution of independent artificial sources without regard to the model parameters. Our prior information on the model parameters is represented by \(p(\mu, \xi)\), and we assume uniform distributions that are also independent of \(\mu, \xi\). We maximized the logarithm of this function with respect to \(\mu\) and \(\xi\) for each of our \(JHK'\) images, to obtain best-fit 1σ sensitivities, and we show our 5σ point-source detection sensitivity as a function of separation from the star in Figure 9. Midplane sensitivities are averaged over both ansae. We show predicted planet brightnesses using models of Burrows et al. (1997) at different ages, allowing inference of detection limits for planet mass.

**REFERENCES**

Aime, C., & Soummer, R. 2004, ApJ, 612, L85
Artyomowicz, P. 1988, ApJ, 335, L79
Augereau, J. C., & Beust, H. 2006, A&A, 455, 987
Augereau, J. C., Nelson, R. P., Lagrange, A. M., Papaloizou, J. C. B., & Mouillet, D. 2001, A&A, 370, 447
Backman, D. E., & Parece, F. 1993, in Protostars and Planets III, ed. E. H. Levy & J. I. Lunine (Tucson: Univ. Arizona Press), 1253
Barrado y Navascués, D., Stauffer, J. R., Song, I., & Caillault, J.-P. 1999, ApJ, 520, L123
Bryden, G., et al. 2006, ApJ, 636, 1098
Burrows, A., et al. 1997, ApJ, 491, 856
Chen, C. H., et al. 2005, ApJ, 634, 1372
———. 2006, ApJS, 166, 351
Cutispoto, G., Messina, S., & Rodonò, M. 2003, A&A, 400, 659
Decin, G., Dominik, C., Waters, L. B. F. M., & Waelkens, C. 2003, ApJ, 598, 636
Dohanyi, J. S. 1969, J. Geophys. Res., 74, 2431
Draine, B. T., & Li, A. 2001, ApJ, 551, 807
Elias, J. H., Frogel, J. A., Matthews, K., & Neugebauer, G. 1982, AJ, 87, 1029
Fitzgerald, M. F., & Graham, J. R. 2006, ApJ, 637, 541
