QM/MM Study of the H₂ Formation on the Surface of a Water Ice Grain Doped With Formaldehyde: Molecular Dynamics and Reaction Kinetics

Boutheïna Kerkeni¹,²,³, Malek Boukallaba², Mariem Hechmi², Denis Duflot⁴ and Céline Toubin⁴*

¹Université de La Manouba, Institut Supérieur des Arts Multimédia de La Manouba, La Manouba, Tunisia, ²Département de Physique, Laboratoire Physique de La Matière Condensée (LPMC) Faculté des Sciences de Tunis, Université Tunis El Manar, Campus Universitaire, Tunis, Tunisia, ³LERMA, Observatoire de Paris, PSL Research University, CNRS-UMR8112, Sorbonne Universités, UPMC Univ. Paris 06, Meudon, France, ⁴Université de Lille, CNRS, UMR 8523—PhLAM—Physique des Lasers Atomes et Molécules, Lille, France

Formaldehyde has been widely observed in the icy mantle of interstellar grains. H₂CO may be formed from successive hydrogenations of CO and may further contribute to the chemical complexity of the Interstellar medium (ISM) participating to heterogeneous reactions with colliding gas phase atoms. Within this context, Eley-Rideal and Langmuir-Hinshelwood rate constants of H₂ formation on a formaldehyde doped amorphous water ice grain model of the ISM, were computed over a wide temperature range [15–2000 K]. We used classical molecular dynamics (MD) simulations to build the model of the H₂CO doped ice surface. Then we studied theoretically by means of hybrid QM/MM ab initio and molecular mechanics methodology (ONIOM) H atoms abstraction from formaldehyde molecules and the H₂ formation. Specifically, we investigate the reactivity of the gas phase H atom toward one formaldehyde molecule lying at one of the slab surfaces. The reaction path and the energetics are predicted, the mechanism is found to be exothermic by 14.89 kcal/mol and the barrier is 6.75 kcal/mol at the QM level CBS/DLPNO-CCSD(T)//ONIOM/aug-cc-pVTZ. We employ two approaches that take into account tunnelling and non-classical reflection effects by means of the Zero Curvature Tunnelling (ZCT), and the Small Curvature Tunnelling (SCT) which all provided comparable results to predict the kinetics of the reaction path. The rate constants show important quantum tunnelling effects at low temperatures when compared to rates obtained from the purely classical transition-state theory (TST) and from the canonical variational transition state theory (CVT). Corner cutting effects are highlighted in the SCT calculations by 4 to 5 orders of magnitude with respect to ZCT rate constants at low temperatures.

Keywords: astrochemistry, ices, formaldehyde, quantum and classical modelling, reaction rates
1 INTRODUCTION

H₂ molecules are ubiquitous in the Universe and constitute the most abundant species and consequently are the main trigger of dust chemistry which is responsible for the formation of key molecules, such as H₂O, NH₃, and CH₃OH. Detection of H₂ was achieved in the interstellar medium (ISM) via a rocket flight in 1970 (Carruthers, 1970). It has been shown that almost certainly H₂ forms at the surface of dust grains and icy mantles in a variety of interstellar environments (Hollenbach and Salpeter, 1970; Williams et al., 2003; Vidali, 2013; Wakelam et al., 2017). Extensive computational (Katz et al., 1999; Cuppen et al., 2010; Cazaux et al., 2011), and experimental studies (Pirronello et al., 1997; Creighan et al., 2006; Watanabe et al., 2010) over the 20 past years have been conducted. Many focused on testing the role of grain models on the energetics prediction of the chemical routes leading to H₂ formation.

Among the grain models, there appear carbonaceous (Farebrother et al., 2000; Ivanovskaya et al., 2010), and silicate ones (Goumans, 2011; Kerkeni and Bromley, 2013). From the modeling point of view molecular clusters and also periodic slabs were served to mimic interstellar grains (Farebrother et al., 2000; Ivanovskaya et al., 2010; Goumans, 2011; Chaaouni et al., 2012; Navarro-Ruiz et al., 2014; Oueslati et al., 2014; Navarro-Ruiz et al., 2015; Oueslati et al., 2015; Navarro-Ruiz et al., 2016; Song and Kästner, 2017), upon which H₂ formation was investigated. Several experimental techniques e.g., (Latimer et al., 2008; Wakelam et al., 2017) at cryogenic temperatures have been realized to investigate the efficiency of H₂ formation in the laboratory. Given the very low temperatures ≈10 K in dense regions of space, dust grains are covered with layers of icy mantles (Ehrenfreund and Schutte, 2000). These serve as a reservoir for molecular accretion, that would subsequently allow the reagents to thermalize, diffuse and react (Congiu et al., 2014), and finally desorb in a later phase during star formation processes. These formed molecules are detected in warmer diffuse clouds of the interstellar medium. The essential enablers of this rich and complex reactivity at the surface of grains may rely in some cases on radical-radical recombination or the presence of UV irradiation and cosmic rays. Dense molecular clouds regions are however less exposed to radiations, suggesting that the grain may truly act as a catalyst reducing the reaction barriers.

Pure H₂O ice was detected at 3 μm by Gillett and Forrest since 1973 (Gillett et al., 1973), it is the most abundant molecular ice in dense ISM regions. While formaldehyde absorption features in ices were observed in young stellar objects (YSOs) in the 5.7–6 μm region. These detections hint to abundances around 6% with respect to H₂O (Gibb et al., 2004; Boogert et al., 2008).

Formaldehyde (CH₂O) ices are believed to form upon water-CO mixtures hydrogenation (Hiraoka et al., 1994; Hiraoka et al., 2002; Watanabe and Kouchi, 2002; Fuchs et al., 2009; Pirim et al., 2010). Comets are also known to contain water related ices in their cores, and when heated by nearby sources, can participate to a complex chemistry network (Schutte et al., 1993; Bossa et al., 2009; Vinogradoff et al., 2011). Laboratory experiments have tackled thermal evolution of comets in order to understand chemical pathways towards Complex Organic Molecules (COMs) formation (Duvernay et al., 2014).

Despite the past extensive investigations, some uncertainties remain, such as the exact composition of the grain models, and the role of mixed ices in the efficiency of H₂ formation. The chemical mechanisms of H₂ formation and the underlying energetic pathways can be model-dependent, and can in some cases present hindering energetic barriers preventing H₂ formation at the low temperatures of the ISM. It is thus timely to provide a detailed energetic description of the possible reaction mechanisms on each specific grain model. In order to be used by astrochemical models, diffusion barriers, adsorption energies and analytic expressions of rate constants should be predicted.

Hydrogen addition and abstraction from formaldehyde have been investigated computationally with DFT by Goumans (Goumans, 2011), and CCSD (T) (by one of the authors) (Siaï et al., 2016) rate constants predictions in gas phase, and on pure water ice (Song and Kästner, 2017). In Woon (2002), quantum chemical electronic structure calculations of H + H₂CO reaction in gas phase and in the presence of water clusters were lately investigated, the catalytic activity of the ice models was analyzed as a function of the activation energies magnitude and without any kinetic modeling. Song and Kästner (2017), employing a QM/MM model, studied the H₂ formation on an amorphous solid water (ASW) upon which one formaldehyde molecule was adsorbed, and rate constants for both Langmuir-Hinshelwood and Eley-Rideal mechanisms were evaluated with the instanton theory, over the temperature range 60–300 K. On the other hand, Monte Carlo simulations (Cuppen et al., 2009) of formaldehyde formation upon CO hydrogenation on interstellar ice surfaces show that H₂CO molecules are found to predominantly exist in the deeper layers of their ice model. H abstraction and addition reactions were also studied experimentally (Chuang et al., 2016) in mixed CO, CH₃OH, and H₂CO ices, where the authors confirm the occurrence of the product channels leading to CH₃OH through hydrogenation, however successive abstraction reactions lead to the formation of HCO and back to CO molecules.

This study may serve as a useful investigation for further model variants to be explored computationally, and for suggesting possible constraints on new experimental setups relevant to ice models and H₂ formation on icy grains in general.

In the present paper we are specifically interested in studying H₂ formation from a formaldehyde-doped ice sample prepared by Molecular Dynamics techniques. The H abstraction from ice formaldehyde by a free incoming gaseous H atom will be investigated considering both reaction mechanisms:

- The Eley-Rideal (ER) mechanism:
  \[ \text{H(gas)} + \text{H₂CO} \rightarrow \text{H₂(gas)} + \text{HCO} \]

- The Langmuir-Hinshelwood (LH) mechanism:
H (ads) + H₂CO – ice – model → H₂ (ads)+HCO – ice – model

Where H (gas), H₂ (gas) are the free hydrogen atom and molecule respectively in gas phase, while H (ads), H₂ (ads) are the adsorbed species on the grain model.

We use a slab model of formaldehyde doped water ice, and choose a reactive site where an accessible CH₂O molecule can be reached upon reaction. We investigate the reaction energetics for H₂ (gas) formation with QM/MM methodologies. Semi-classical rate constants at a large temperature range are predicted using sophisticated Variational Transition State Theory (VTST) (Fernandez-Ramos et al., 2007), that allow unlike other methods to compute rate constants for temperatures above the cross over temperature T_c and also at very low temperatures ≈15 K characteristic of dense regions in the ISM where molecules are believed to form. We compare our results to available data from the literature and investigate the role of the present model grain and computational methodologies on the prediction of the energetics and the rate constants. In Computational Details we describe the methodology to generate the doped ice slab, the adopted computational methods for electronic structure and rate constants calculations. Results and their implications are discussed in Results and Discussion. Finally, the main results are put into perspective in Conclusion.

2 COMPUTATIONAL DETAILS

2.1 Classical Molecular Dynamics Calculations

The mixed formaldehyde/water ice was generated by classical molecular dynamics calculations using the Gromacs code (Abraham et al., 2015). The water molecules were described with the TIP4P/2005 model that proved to reproduce fairly well ice along the phase diagram (Abascal and Vega, 2005; Michoulier et al., 2018). OPLS force field (Jorgensen et al., 1983; Cornell et al., 1995) was employed for the formaldehyde molecules. The combination of OPLS and water models derived from TIP4P has been validated in Refs. (Collignon and Picaud, 2004; Ballenegger et al., 2006). The equations of motion were integrated by the leapfrog algorithm with a 1 fs time step. The Lennard-Jones and the short-range part of the Coulomb interactions were truncated at 10 Å. The long-range part of the Coulomb interaction was evaluated using the smooth particle-mesh Ewald method with a relative tolerance of 10⁻⁵, fourth-order cubic interpolation and a Fourier spacing parameter of 0.12. Water and formaldehyde molecules were treated as rigid bodies using the SETTLE algorithm.

Amorphous ice was doped with formaldehyde at the ratio 20 H₂CO:1000 H₂O (Pontoppidan et al., 2004). The slab is formed from 20 CH₂O randomly distributed in a box containing 1000 H₂O molecules. In order to favor diffusion of the molecules, an annealing procedure is carried out in the NPT ensemble using a Berendsen thermostat, heating the sample from 100 to 300 K and then cooling it back to 110 K for a total duration of 10 ns. The obtained box, of dimensions 26 × 30 × 35 Å, is then elongated along the z direction to form two interfaces exposed to vacuum. The resulting box cell dimensions are 26 × 30 × 100 Å. A final equilibration in the NVT ensemble was then performed at 110 K during 10 ns. A side view of the doped ice sample is shown in Figure 1A. The amorphous character of water was insured by checking the water density as shown in Figure 1B. Moreover, the

H₂ (ads) + H₂CO – ice – model → H₂ (gas) + HCO – ice – model

FIGURE 1 | (A) Side view of the doped ice slab. Water is represented in light colors and CH₂O by van der Waals spheres. The picked surface CH₂O molecule is highlighted by a red circle. (B) Atomic distributions in arbitrary units along the z direction of the Oxygen atoms of H₂O (OW) or Carbon atoms of CH₂O (C). For a better visualization, Carbon density has been multiplied by a factor 10.
compacity and low porosity of the ice are not affected by the presence of the organic molecules, the density of the ice slab is only changing from 0.955 g/cm³ for pure amorphous ice to 0.989 g/cm³ for our doped ice sample. H₂CO molecules are distributed all over the slab but few of them remain at the surface. The abstraction reaction is subsequently studied from one of these surface formaldehyde molecules within a QM/MM scheme. It should be noted that at the low concentration considered here, the mutual interactions between H₂CO molecules is screened by water molecules. The water network is also only slightly affected by the presence of the H₂CO molecules.

### 2.2 Quantum Chemical Calculations

Because of its amorphous nature and large molecular size, the whole system cannot be studied within a quantum mechanical treatment. Therefore, it has been divided into two parts. The first one, where the electronic energy of the system is calculated with an ab initio framework (QM), is located around the site where the reaction occurs. On the other hand, classical mechanics methods (MM) were used for the rest of the icy layer.

We employ the hybrid QM/MM ONIOM methodology (Chung et al., 2015) where the active species involved in the reaction process, i.e., H, CH₂O and 10 H₂O within a 4 Å radius of the CH₂O molecule are studied with the hybrid meta-GGA functional M05-2X (Zhao et al., 2006) combined with an augmented correlation-consistent polarized valence basis set of Dunning namely, the aug-cc-pVTZ (Dunning, 1989; Kendall et al., 1992). This approach satisfactorily predicts the geometry and is particularly suitable for treating weak interactions as well as for providing accurate activation energy barriers (Hohenstein et al., 2008; Leverentz et al., 2013; Sirianni et al., 2018). M05-2X has been tested to perform in a similar way as M06-2X in the case of hydroxylated pyroxene clusters (Kerkeni et al., 2019). The rest of the system, i.e., the icy grain minus CH₂O + 10H₂O is treated with the Amber MM force field. The mechanical embedding scheme (Chung et al., 2015) was employed for all calculations. For open-shell structures, unrestricted wave functions were employed. All the DFT quantum chemical calculations were performed with the Gaussian 16 code (Frisch et al., 2016).

Initially the CH₂O + 10H₂O molecules in the QM region were allowed to relax in a QM/MM calculation, the final structure was afterwards used while freezing the 10 H₂O molecules. Therefore, the reactive H and CH₂O fragments were allowed to relax without any constraint during the reaction mechanism. The remainder of the grain model was kept frozen during all calculations. Geometry optimizations were carried out using the default Gaussian convergence thresholds. The nature of the stationary points of the potential energy surface (PES), minimum or saddle point, was checked by computing unscaled harmonic frequencies. Transition states (TSs) were searched for using the Berny algorithm (Schlegel, 1982). The Minimum Energy Path (MEP) was computed using the Intrinsic Reaction Coordinate (IRC) method (Fukui, 1981; Hratchian and Schlegel, 2005) with a gradient step size of 0.01 a₀/(amu)½. For 46 points along each side of the MEP, the harmonic frequencies were computed at the M05-2X/aug-cc-pVTZ/Amber level. The MEP energies were finally corrected by adding the unscaled zero-point vibrational energy (ZPE), leading to the vibrational adiabatic potential energy V_a.

In order to obtain more accurate energies at an affordable cost, the DFT results were improved using a methodology recently used to obtain accurate binding energies of atoms and small molecules at the surface of both crystalline and amorphous ices (Duflot et al., 2021). To this end, the optimized geometries of the QM zone for all stationary and IRC points were recovered. The resulting cartesian coordinates were then used as inputs for a CBS/DLPNO-CCSD(T) (Guo et al., 2018) single point calculation, using the ORCA code (Neese, 2018; Neese et al., 2020). Resolution of the identity (RIJK) was used (Weigend et al., 2009) with the auxiliary basis set from Weigend (Weigend, 2008). For DLPNO-CCSD(T), the normal criteria were used as discussed by Liakos et al. (2015). The frozen core approximation was also used so carbon and oxygen 1 s orbitals were not included. The auxiliary basis set for correlation is taken from Hellweg et al. (2007). For Complete Basis Set (CBS) extrapolation, def2-TZVPP and def2-QZVPP basis sets were employed (Weigend and Ahlrichs, 2005). The Hartree-Fock and the correlation energies were extrapolated separately as shown in (Neese and Valeev, 2011) with a = 7.880 for Hartree-Fock and β = 2.970 for correlation. Interestingly, the T₁ diagnostic (Lee et al., 1995) remains small along the path, with a maximum value of 1.2% at the TS geometry, thus confirming the absence of multireference character to the wavefunction. This diagnostic was slightly larger for gas phase species, peaking at 2.4% for the TS. By replacing the energy part of the total ONIOM calculation by the CBS/DLPNO-CCSD(T) energies, a new ONIOM extrapolated energy is obtained. On the other hand, the DFT frequencies and the resulting ZPE values were kept unmodified. This procedure was applied on the stationary and all the IRC points along the calculated reaction path.
2.3 Reaction Kinetics

Conventional Transition State Theory

The conventional transition-state theory rate constant is the product of a symmetry number by $k_B T/h$ multiplied by the ratio of a partition function evaluated at $k_B T$ to one evaluated at the reactant, times an exponential decay of the classical barrier height as in Eq. 3. The partition functions are evaluated as products of electronic and vibrational partition functions. As we are dealing with surface reactions, we discard the relative translational partition function per unit volume and the rotational ones.

The conventional transition state-theory rate constant, $k_{TST}(T)$, is given by the following expression (Truhlar et al., 1985):

$$k_{TST}(T) = \frac{k_B T}{h} \frac{Q_f^R(T)}{Q_r^R(T)} \exp[-\Delta V_a/(k_B T)]$$

where $\Delta V_a$ is the forward classical barrier height, $h$ is the Planck constant, and $k_B$ is the Boltzmann constant. $Q_f^R$ and $Q_r^R$ are the TS and the reactant partition functions, respectively, which are relevant to internal vibrational motions, and the electronic distribution. All vibrational modes are treated as separable harmonic oscillators.

Canonical Variational Transition State Theory

Canonical variational transition-state theory (CVT) (Liu et al., 1993) has been used to estimate the rate constants. The canonical variational, transition state theory rate constant $k_{CVT}$ is obtained by finding the location of the minimum flux through the transition state at a given temperature. Note that in using a free energy of activation criterion to determine the location of the variational transition state, both entropic and energetic contributions are taken into account. We may write:

$$k_{CVT}(T) = \min_k k^G(T, s^*_CVT) = k^G(T, s^*_CVT(T))$$

where $k^G(T, s) = \frac{k_B T}{h} \frac{Q_f^R(T,s)}{Q_r^R(T)} \exp[-\frac{\Delta V^{AG}(s)}{k_B T}]$.

$V_{MEP}(s)$ is the classical potential along the minimum path (MEP) referenced to the reactant energy, $s$ is the mass scaled reaction coordinate, and $s^*_CVT$ is the location of the canonical transition state on the reaction path, i.e., where the flux is minimal. $s = 0$ corresponds to the transition state; at the reactant $s$ is a finite negative number, while for the product $s$ is a finite positive number.

Semiclassical Reaction Probabilities

Light atoms such as hydrogen tunnel through barriers that cannot be surmounted classically. This quantum effect can be important at low temperatures. The exponential damping of wave tunnelling through a given barrier leads to the tunnelling probability $P(E)$ at total energy $E$:

$$P(E) = \exp[-2\theta(E)]$$

where $\theta(E)$ represents the amount of exponential decay. This function may be obtained in several ways.

Zero Curvature Tunnelling Method

When the reaction path curvature can be neglected, the proper tunnelling path is the MEP. For tunnelling along the MEP, $\theta(E)$ is the imaginary action integral given by:

$$\theta(E) = h^{-1} \int_{s_0}^{s_1} ds [2\mu(V^G_a(s) - E)]^{1/2}$$

$V^{AG}$ is the maximum of the ground state vibrational adiabatic potential energy:

$$V^{AG} = \max_s V^G_a(s) = V^G_a(s = s^{AG})$$

where $V^G_a(s) = V_{MEP}(s) + ZPE(s)$, $V_{MEP}$ is the classical potential energy of the MEP and ZPE is the zero-point energy correction relevant to the frequencies orthogonal to the reaction path. The $s_0$ and $s_1$ are the reaction coordinates of the classical turning points in the reactant and product valleys, respectively.
and μ is the reduced mass. This approach is called the zero curvature tunnelling (ZCT) method (Skodje et al., 1981).

In the ZCT approach, tunnelling is calculated from the semiclassical (i.e., WKB) ground-state transmission coefficient κ(T) (Skodje et al., 1981):

\[ k_{ZCT}(T) = \kappa_{ZCT}(T) \times k_{TST}(T) \]

The transmission coefficient κ is temperature dependent, which takes into account tunnelling and non-classical reflection effects, κ(T) is given by

\[ \kappa(T) = \exp\left[-\frac{\theta}{\kappa_3}dE\right] \int_{V(\mu=0)}^{\infty} \exp\left[-\frac{\theta}{\kappa_3}dE\right] \]

Small Curvature Tunnelling Method
Liu et al. (1993) have reported that tunnelling probabilities may increase because of the corner-cutting effect, which is not accounted for in the ZCT method. More advanced tunnelling methods are based on the inclusion of deviations between the tunnelling path and the reaction path (Vandeputte et al., 2010). In the present work, the centrifugal dominant small curvature semiclassical adiabatic ground state (CD-SCSAG) tunnelling method (Lu et al., 1992; Liu et al., 1993) is applied, where the effect of the reaction curvature is included by replacing the reduced mass μ by an effective mass μ_eff (Liu et al., 1993). The tunnelling probability at energy E is:

\[ P(E) = \frac{1}{1 + \exp(\frac{-\beta(E)}{k_B T})} \]

where \( \theta(E) \) is the imaginary action integral along the tunnelling path as in Eq. 6. κ(T) is calculated as in Eq. 9 and the thermal rate constant is tunnelling corrected in the corresponding way as done for ZCT.

The TST, CVT, CVT/ZCT and the CVT/SCT rate constants are computed using the POLYRATE program, version 2010-A (Zheng et al., 2010). The CVT rates were fitted using the analytical expression proposed by Zheng and Truhlar (2010):

\[ k(T) = a\left(\frac{T}{300}\right)^\beta \exp\left[-\frac{\gamma(T + T_0)}{T^2 + T_0^2}\right] \]

where a, β, γ and T_0 are constants optimized to match the calculated rates.

### 3 RESULTS AND DISCUSSION

#### 3.1 Gas Phase Abstraction

In order to validate the methods employed in the ONIOM calculations, namely M05-2X/aug-cc-pVTZ and CBS/DLPNO-CCSD(T), we have employed them to calculate the gas phase reactions. It should be kept in mind that the CBS single point calculations were performed at the M05-2X geometries and ZPE is evaluated at this DFT level too. The results are compared to previous works (Goumans, 2011; Ruscic, 2015; Siaï et al., 2016; Song and Kästner, 2017) in Table 1. The computed energetics given in this table are the exothermicity (ΔE) and the vibrational adiabatic barrier (ΔV_a) between the transition state and the reactants and between the products and the reactants, respectively. The corresponding ZPE-corrected values are labelled by a star symbol.

| Species | CO  | CH  | CH_b | ∠HCO | ∠HbCO | H_bH_a | ∠H_bH_a | ∠H_bCH_b |
|---------|-----|-----|------|------|-------|--------|---------|----------|
| H_2CO   | 1.2012 | 1.0983 | 1.0968 | 121.4 | 121.9 | —      | 116.7 | —        |
| TS      | 1.1847 | 1.1006 | 1.2567 | 124.5 | 120.6 | 1.0683 | 114.9 | 1.4      |
| HCO     | 1.1716 | 1.1092 | —     | 125.3 | —     | —      | —      | —        |
| H_2     | —   | —   | —    | —    | —     | 0.7379 | —      | —        |

---

TABLE 2 | Molecular geometry parameters of the fragments [bond lengths (Å) and angles (°)] at the M05-2X/aug-cc-pVTZ level. H_b is the abstracted atom, while H_a is the incoming atom.
TABLE 3 | Calculated harmonic vibrational frequencies (in cm\(^{-1}\)) and zero-point energies (in Hartrees) for the stationary points.

| Species | Frequencies | ZPE |
|---------|-------------|-----|
| H\(_2\)CO | 42, 53, 68, 91, 151, 198, 1246, 1285, 1553, 1845, 3015, 3106 | 0.028822 |
| TS | 71737, 40, 46, 48, 94, 99, 136, 341, 440, 1184, 1223, 1232, 1405, 1891, 3024 | 0.025724 |
| HCO | 36, 52, 62, 82, 137, 298, 1132, 1968, 2876 | 0.015134 |
| H\(_2\) | 4533 | 0.010327 |

TABLE 4 | Comparison between ER and LH ZPE-corrected energies (kcal/mol).

| Species | ER DFT | CBS DFT | LH DFT | CBS |
|---------|--------|---------|--------|------|
| H\(_2\) | -11.47 | -12.79 | -11.52 | -11.46 |
| H\(_2\)CO | -13.57 | -14.89 | -13.00 | -13.18 |
| HCO | 10.21 | 8.68 | 8.74 | 8.41 |
| H\(_2\) | 8.28 | 6.75 | 7.23 | 6.52 |

Figure 4 | Product geometry (limited to QM zone).

3.2 Reaction Mechanisms on the Model Grain
3.2.1 Stationary Points
We initiated the reaction process by the reactive collision of one single gaseous H atom with an already adsorbed CH\(_2\)O molecule dangling at the doped ice grain surface (Figure 2). The present geometry is similar to the most abundant one obtained by Song and Kästner on pure ASW ice (see Figure 1A in ref. (Song and Kästner, 2017)). It is worth mentioning that in ref (Song and Kästner, 2017) a single formaldehyde molecule was adsorbed on their ice models. In the present model, the reactive formaldehyde oxygen atom forms a hydrogen bond with the nearest water hydrogen atom with a length of about 2.00 Å, close to the 1.90 Å value obtained by Song and Kästner. A value of 1.88 Å was also obtained at BHLYP/6-311++G (d,p) level on a 18-water cluster by Rimola et al. (Rimola et al., 2012). The search of the transition state corresponds to the geometrical configuration where the hydrogen in CH\(_2\)O is abstracted by the incoming H atom (Figure 3 and Table 2). At the transition state the CO bond is shortened by \(\approx 0.017\) Å with respect to the reactant one (see Figure 3 and Table 2). Table 3 displays the calculated frequencies, showing the 6 low-value modes corresponding to the motion of the H\(_2\)CO and TS structures with respect to the surface. When the H atom abstraction occurs, H\(_2\) forms with an equilibrium distance of 0.738 Å, and the distance from the carbon to the abstracted H is 2.32 Å, the CHH angle being \(\approx 177°\). The abstraction process is thus quasi-collinear, very much like in the gas phase case (Siaï et al., 2016) and on pure ASW ice (Song and Kästner, 2017). The relevant geometrical parameters are given in Figure 4 and Table 2 for all involved species in the reaction mechanism. The calculated H-H distance at the TS (1.068 Å) is slightly larger than the 1.022 Å obtained by Song and Kästner (2017).

All attempts to locate reactive and product Van der Waals complexes failed. Song and Kästner (2017) mention a complex with an energy very close to the reactants but no details are given about its geometry. In the gas phase case (Siaï et al., 2016), it was concluded that the product complex was electronically unstable after including BSSE effects. The reactant complex, with the incoming H atom at about 3.35 Å, lies very close to the reactant (-023 kcal/mol at CCSD(T) level) and did not play any significant role in the dynamics study of the abstraction reaction.

Figure 5 shows a comparison between the geometries of the stationary points and the last points of the IRC calculations. Beyond these geometries, the IRC calculation stops due to the stability of the energy. On the reactant side, at CBS level, the last IRC point lies 0.23 kcal/mol with ZPE) above the energies of the isolated grain + H system. This suggests that the reaction barrier for the Eley-Rideal mechanism would be 0.23 kcal/mol higher than that for the Langmuir-Hinshelwood one (see Table 4). The H\(_2\) is at \(\approx 3.4\) Å from the CH\(_2\) closest hydrogen. On the other side, the last IRC point is 1.71 kcal/mol above the isolated products (see also Figure 6). The closest H atom of H\(_2\) is \(\approx 2.8\) Å from the carbon atom. For both cases there remains a large difference between the orientation of the isolated H\(_2\)CO (Figure 5A) or HCO (Figure 5B) molecules compared to the last IRC point, which proves that the convergence of the MEP...
calculation has already reached local minima in both sides. The same behavior is also found for the TS as shown in Figures 5C & 5D, where one can see the orientation of the reactant and product compared to the TS. Several attempts were made to determine whether isolated reactant and product geometries were in fact local minima and not connected to the IRC path. For example, the geometry optimization was restarted using the final IRC geometries by removing the H and H2 molecules. In all cases, the minima were found to be the same as obtained independently (as shown in Figures 2, 4). This suggests that the TS and the MEP are common to the ER and LH mechanisms. There are several possibilities to explain these results. First, the presence of an H atom or an H2 molecule even at rather large distances has a strong enough influence to re-orient the H2CO and HCO molecules with respect to the surface. Nevertheless, the PES is rather flat too. Finally, the fact that the surrounding water molecules are frozen may have also some minor impact on the geometries.

Table 1 shows the comparison between the ONIOM energies of the stationary points using the two levels of calculations [M05-2X/aug-cc-pVTZ and CBS/DLPNO-CCSD(T)]. The same trends found in gas phase occur, namely that the exothermicity decreases when going from M05-2X to CBS (−11.47 to12.79 kcal/mol for ΔE). On the other hand, the barrier height is reduced, from 8.28 to 6.75 kcal/mol. It is also possible to compare the values of these properties to those obtained in gas phase with the same methods. As can be seen in Table 1, the exothermicity is larger in gas phase for both methods, while the barrier height is only slightly larger. This would certainly result in gas phase rate constants being somehow larger at small temperatures than those obtained from the grain model. Thus, the ice model yields a noticeable stabilization of the gas-phase TS with respect to the effect on the minima. Song and Kästner (2017), at the PW6K-D3/def2-TZVP level, found the same behavior going from gas phase to pure ASW surface, i.e., an augmentation of the barrier height by about 1 kcal/mol and a reduction of the exothermicity (Table 1). This latter reduction is somewhat larger in Song and Kästner (2.41 kcal/mol) compared to the present result (1.01 kcal/mol).
Another interesting quantity which can be obtained from the present calculations is the binding energy (BE) of the reactants and products to the ice surface [see also (Duflot et al., 2021)]. We define the BE of a molecule M on the icy grain as the positive quantity:

$$\text{BE} = -[E(\text{ice} + M) - E(\text{ice}) - E(M)]$$  \hspace{1cm} (12)$$

where $E(\text{ice} + M)$ is the energy of the adsorbed molecule M on the icy grain, $E(M)$ is the energy of M in the gas phase and $E(\text{ice})$ is the energy of the bare icy grain. The calculations are performed with the QM/MM procedure detailed above, and include ZPE from DFT. For H$_2$CO, BE is found to be 9.18 kcal/mol at DFT level and 8.38 kcal/mol at CBS level. At the PWB6K-D3/def2-TZVP/MM level (without ZPE), Song and Kästner (2017) found a broad distribution of BE's on ASW, between about 2.0 and 18.6 kcal/mol. The distribution was centered on BE between about 8.0 and 9.9 kcal/mol. These authors selected one ASW structure upon which they calculated the rates with a BE of about 9.14 kcal/mol. Finally, our QM/MM BE value lies within accordance with their BE distribution.

For HCO, the DFT and CBS values we computed are 8.08 and 7.37 kcal/mol, respectively. For this latter species, the CBS values can be compared to the largest BE's obtained on pure crystalline (7.08 kcal/mol) and amorphous (5.67 kcal/mol) ices (Duflot et al., 2021). However, it should be kept in mind that in the present work, the ice surface was not allowed to relax in reactivity studies, and that in ref (Duflot et al., 2021) the ice...
3.2.2 Minimum Energy Path

Figure 6 displays the variation of the classical potential energy \( V_{\text{MEP}} \) as a function of the reaction coordinate \( s \) for the reaction studied here on the ice grain. The CBS \( V_{\text{MEP}} \) curve is flatter than the DFT one on the reactant side. The reduction of the barrier height is visualized via the crossing of the CBS and DFT curves. Unlike the gas phase case where the \( V_{\text{MEP}} \) curve presents a discontinuity at \( s = -0.25 \text{ amu}^{1/2} \text{ bohr} \) [see Figure 1 in (Siaï et al., 2016)], due to the single point CCSD(T)//MP2 level, the present DFT and CBS \( V_{\text{MEP}} \) profiles are more regular. The CBS \( V_{\text{MEP}} \) curve displays two small bumps at about \( s = 0 \) and \( s = 0.27 \text{ amu}^{1/2} \text{ bohr} \), separated by a small well at \( s = 0.15 \text{ amu}^{1/2} \text{ bohr} \). The inclusion of ZPE corrections does not change the position of the maximum of the curve which remains very close to \( s = 0 \text{ amu}^{1/2} \text{ bohr} \). The \( \Delta V_{\text{ZPE}} \) curve shows the evolution of the vibrational frequencies, using the TS as a reference: around the TS, i.e., between \( s = 0.2 \) and \( s = -0.3 \text{ amu}^{1/2} \text{ bohr} \), the variation remains close to 0. Then a steep variation occurs and rapidly leads to the asymptotic values corresponding to the formation of the formaldehyde CH bond (left side) and the formation of the \( \text{H}_2 \) bond (right side).

3.2.3 Kinetic Study: \( \text{H}_2 \) Formation Mechanisms

**Eley-Rideal Mechanism**

Figure 7A displays the calculated rates for the Eley-Rideal mechanism, compared to the analytical functions fitted using Eq. 11 and the results from Song and Kästner (2017). It should be kept in mind that Song and Kästner used instanton theory (Zaverkin and Kästner, 2020) between 59 K and the so-called crossover temperature (Atfleck, 1981) \( T_c = 366 \text{ K} \) and variational TST for higher temperatures up to 1000 K. Also, in Eq. 11, the \( \beta \) parameter was set to 1.0 in ref. (Song and Kästner, 2017). In the present work, \( \beta \) was optimized and the temperature spans a broader interval (15–2000 K). The fitted parameters for CVT rates are shown in Table 5 and compared to Song and Kästner. From Figure 7A, it is clear that Eq. 11 fits very well both ZCT and SCT rates. At very high temperatures, tunnelling effects are small (e.g., \( \kappa \approx 1.1 \) at 2000 K for both ZCT and SCT). However, at room temperature, tunneling effects are still important with \( \kappa_{\text{ZCT}} = 16.8 \) and \( \kappa_{\text{SCT}} = 34.0 \). As recently pointed out by Richardson (2018), when the TS imaginary frequency is larger than \( 1300 \text{ cm}^{-1} \), deep-tunnelling still occurs at this temperature. This is indeed the case in the present work since the TS imaginary frequency is \( 1737 \text{ cm}^{-1} \) (Table 3). This gives a cross-over temperature of \( T_c \approx 400 \text{ K} \), which is very similar to that of Song and Kästner (2017). At low temperatures, the CVT/ZCT rates appear to be several orders of magnitude lower than the CVT/SCT, which is a common trend (Truhlar and Kuppermann, 1971; Liu et al., 1993), due to the corner cutting effects (Allison and Truhlar, 1998). Our CVT/SCT curve is thus closer to Song and Kästner’s one than the CVT/ZCT one. There remains however a difference of several orders of magnitude as can be seen in Table 6, between the present rates and the values provided by Song and Kästner for selected temperature values. The differences are due to the different barrier heights, IRC shape and theoretical models used to compute the rates. These differences are also reflected in Table 5: there is a large difference between the ZCT and SCT fitted parameters. Furthermore, \( \beta \) is significantly different from 1 in our case.

**Langmuir-Hinshelwood Mechanism**

In Figure 7B, the calculated rate constants obtained for the LH mechanism are shown together with Song and Kästner (2017)’s...
fitted rate function. As in the ER case, the CVT/ZCT and CVT/SCT curves were fitted using Eq. 11. The optimized parameters are given in Table 5. Most of the trends observed in the ER case, such as the importance of tunnelling at high and low temperatures and the difference between the ZCT and SCT results, are also observed. The main difference comes from the comparison between the present CVT/SCT rate and Song and Kästner’s one: both curves appear to be very close, especially at low temperature. This is reflected in the fitted parameters given in Table 5: although our α value is about 40 times larger, the other parameters remain very similar. In contrast to our ER results, β is now very close to 1. Table 6 also shows that the rates differ by a factor of around 3 at all selected temperatures. The similarity with Song and Kästner’s results may be rationalized by the closeness of our LH barrier (Table 4) compared to ref (Song and Kästner, 2017). Indeed, these authors calculated the LH rates using a complex with a barrier of 3030 K or 6.02 kcal/mol, virtually identical to the ER barrier. As shown in Table 4, our LH barrier is very close to this value (6.52 kcal/mol at the CBS level). Given the large rate coefficients predicted in the LH mechanism even at T = 15 K, it is anticipated that besides the exothermicity of the reaction process, the reaction mechanism is in favor of the formation of gaseous H2 molecules. However, even though our ice model is intended to mimic ISM conditions, we would expect that diffusion of the incoming H (gas) atoms, so that they meet one CH2O on the grain, will be the rate limiting step.

4 CONCLUSION

In the present work, we have employed Density Functional Theory for geometry optimization, ZPE calculations, and CBS/DLPNO-CCSD(T)//ONIOM/aug-cc-pVTZ single point energies methods on a large-scale system derived from a classical molecular dynamics trajectory. These calculations serve indeed as a feasibility assessment of previously benchmarked DFT (and to some extent, CVT) methods for the study of chemical reactions.

We study the abstraction reaction between an incoming gas phase hydrogen atom and another hydrogen atom belonging to a formaldehyde molecule at the surface of a mixed formaldehyde/water icy grain. The size of the system required the use of hybrid QM/MM techniques to obtain the detailed shape of the full reaction pathway including the effect of the environment. The entire minimum energy path was computed with CBS and M05-2X zero-point energy inclusion for each stationary point.

These results were then used to obtain the rate constants of this reaction between 15 and 2000 K for both ER and LH mechanisms using methods more sophisticated than the usual transition state theory, including contributions from variational and tunnelling effects. This work provides new results with respect to the choice of the model grain, i.e., doped formaldehyde-H2O amorphous ice, to the application of CBS model chemistry as opposed to pure DFT treatments, and to the use of VTST over a larger temperature range than what was reported previously. Our calculations show that both reaction models (ER and LH) exhibit exothermic pathways.

The present work focused on the H abstraction of H2CO and formation of H2, but the H2CO + H reaction has actually several possible products, such as H2COH, H2COH. Using the proposed methodology to characterize the latter products formation through reactions at the grain surface would definitively be of interest and complementary to the present work.

In addition, the reaction was fully characterized for one configuration that was arbitrarily chosen along a classical molecular dynamics trajectory. It can be expected that various binding sites may exist on the surface characterized by different environments around the surface CH2O molecule. To confirm the trend, a sampling should be carried out over a variety of binding sites. However, a full characterization of the reaction path, as presented here, has to be carried out for each binding environment, such an investigation certainly requires a substantial computational effort.

Finally, the reaction was characterized on a mixed grain, the reacting CH2O molecule forming part of the doped ice model. This work proposes a methodology to account for the presence of impurities in interstellar ices. Further efforts are needed to quantify more precisely the influence of these dopants on reaction rate constants both in terms of molecular or atomic diversity and concentration of the species.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

DD did some of the quantum chemical calculations, data curating and wrote parts of the manuscript. BK performed all DFT calculations, and reaction rates, and provided a first draft of the paper. MB prepared the QM/MM input structures for Gaussian calculations. MH performed the MD calculations. CT supervised the MD calculations and participated in the data curating.

ACKNOWLEDGMENTS

The authors thank the PCMI (Programme National de Physique et Chimie du Milieu Interstellaire) for support and the Centre de Ressources Informatiques (CRI) of the Université de Lille for providing computing time. MH acknowledges Dr C. Fotsing-Kwetché and Dr E. Michoulier for their help on the Molecular Dynamics part. MH acknowledges the Ministry of Higher Education and
**REFERENCES**

Abascal, J. L. F., and Vega, C. (2005). A General Purpose Model for the Condensed Phases of Water. *TIP4P/2005*. *J. Chem. Phys.* 123, 234505. doi:10.1063/1.212687

Abraham, M. J., Murtola, T., Schulz, R., Páll, S., Smith, J. C., Hess, B., et al. (2015). 2020 HPC resources from GENCI-TGCC (Grant No. CGR15-0381). *Frontiers in Astronomy and Space Sciences* | www.frontiersin.org March 2022 | Volume 9 | Article 807649

Allison, T. C., and Truhlar, D. G. (1998). Gaussian Basis Sets for Use in Correlated Molecular Calculations. *J. Chem. Phys.* 108, 11443–11462. doi:10.1063/1.475081

Cuppen, H. M., van Dishoeck, E. F., Herbst, E., and Tielens, A. G. G. M. (2009). *H2 Reformation in post-AGB Stars*. *Astron. Astrophys.* 508, 257–287. doi:10.1051/0004-6361/200913119

Boogert, A. C. A., Pontoppidan, K. M., Knez, C., Lahuis, F., Kessler-Silacci, J., van Dishoeck, E. F., et al. (2008). The c2dSpitzerSpectroscopic Survey of Ices Around Low-Mass Young Stellar Objects. *I. H2O and the 5-8 μm Band*1.2. *Astrophysical J.* 678, 985–1004. doi:10.1086/533425

Bossa, J. R., Theule, P., Duvernay, F., and Chiavassa, T. (2009). NH2CHO Thermal Formation in Interstellar Ices Contribution to the 5-8 μm Region Toward Embedded Protostars. *Astrophysical J.* 707, 1524–1532. doi:10.1088/0004-637X/707/2/1524

Carruthers, G. R. (1970). Rocket Observation of Interstellar Molecular Hydrogen. *Astrophysical J.* 161, L81. doi:10.1086/180575

Charbonneau, H., Bergeron, H., Baouche, S., Dufieux, F., Matar, E., Congiu, E., et al. (2012). Sticking Coefficient of Hydrogen and Deuterium on Silicates under Interstellar Conditions. *Astron. Astrophysics* 538, A128. doi:10.1051/0004-6361/201117220

Chuang, K.-J., Fedoseev, G., Ioppolo, S., van Dishoeck, E. F., and Linnartz, H. (2016). H-atom Addition and Abstraction Reactions in Mixed CO, H2CO and CH3OH Ices - an Extended View on Complex Organic Molecule Formation. *Monthly Notices R. Astronomical Soc.* 455, 1702–1712. doi:10.1093/mnras/stw2288

Chung, L. W., Sameera, W. M. C., Ramozzi, R., Page, A. J., Hatanaka, M., Petrova, G. P., et al. (2015). The ONIOM Method and its Applications. *Chem. Rev.* 115, 5678–5796. doi:10.1021/acs.chemrev.5b00419

Collignon, B., and Picaud, S. (2004). Comparison between Methanol and Formaldehyde Adsorption on Ice: a Molecular Dynamics Study. *Chem. Phys. Lett.* 393, 457–463. doi:10.1016/j.cplett.2004.06.085

Congiu, E., Minissale, M., Baouche, S., Chaabouni, H., Moudens, A., Cazaux, S., et al. (2014). Efficient Diffusive Mechanisms of O Atoms at Very Low Temperatures on Surfaces of Astrophysical Interest. *Faraday Discuss.* 168, 151–166. doi:10.1039/C4FD00002A

Cornell, W. D., Cieplak, P., Bayly, C. I., Gould, I. R., Merz, K. M., Ferguson, D. M., et al. (1995). A Second Generation Force Field for the Simulation of Proteins, Nucleic Acids, and Organic Molecules. *J. Am. Chem. Soc.* 117, 5179–5197. doi:10.1021/ja00124a002

Creighan, S. C., Perry, J. S. A., and Price, S. D. (2006). The Rovibrational Distribution of H2 and HD Formed on a Graphite Surface at 15–50 K. *J. Chem. Phys.* 124, 114701. doi:10.1063/1.2174878

Cuppen, H. M., Kristensen, L. E., and Gavardi, E. (2010). H2 Reformation in post-Shock Region. *Monthly Notices R. Astronomical Soc.* Lett. 406, no.–L15. doi:10.1111/j.1745-3933.2010.00871.x

Cuppen, H. M., van Dishoeck, E. F., Herbst, E., and Tielens, A. G. G. M. (2009). Microscopic Simulation of Methanol and Formaldehyde Ice Formation in Cold Dense Cores. *Astron. Astrophysics* 508, 257–287. doi:10.1051/0004-6361/200913119

Duffot, D., Toubin, C., and Monnerville, M. (2021). Theoretical Determination of Binding Energies of Small Molecules on Interstellar Ice Surfaces. *Front. Astron. Space Sci.* 8, 645243. doi:10.3389/fspas.2021.645243

Dunning, T. H., Jr. (1989). Gaussian Basis Sets for Use in Correlated Molecular Calculations. I. The Atoms boron through Neon and Hydrogen. *J. Chem. Phys.* 90, 1007–1023. doi:10.1063/1.456153

Duvernay, F., Rimola, A., Theule, P., Danger, G., Sanchez, T., and Chiavassa, T. (2014). Formaldehyde Chemistry in Cometary Ices: the Case of HOCH2OH Formation. *Phys. Chem. Chem. Phys.* 16, 24200–24208. doi:10.1039/C4CP03031A

Ehrnfreund, E., and Schutte, W. A. (2000). ISO Observations of Interstellar Ices: Implications for the Primacy of Comets. *Adv. Space Res.* 25, 2177–2188. doi:10.1016/S0273-1177(99)01151-5

Farbreather, A. J., Meijer, A. J. H. M., Clancy, D. C., and Fisher, A. J. (2000). Formation of Molecular Hydrogen on a Graphite Surface via an Eley-Rideal Mechanism. *Chem. Phys. Lett.* 319, 303–308. doi:10.1016/S0009-2614(00)00128-7

Fernandez-Ramos, A., Ellingson, B. A., Garrett, B. C., and Truhlar, D. G. (2007). *Variational Transition State Theory with Multidimensional Tunneling - Fernandez-Ramos - 2007 - Reviews in Computational Chemistry*. Wiley Online Library. Available from: https://onlinelibrary-wiley-com.ressources-electroniques.univ-lille.fr/doi/10.1002/9780470164493.ch3 (accessed September 27, 2021).

Frisch, M. J., Trucks, G. W., Schlegel, H. B., Scuseria, G. E., Robb, M. A., Cheeseman, J. R., et al. (2016). *Gaussian 16*. Wallingford, CT: Rev. B.01.

Fuchs, H., Brauers, T., Häselig, R., Holland, F., Mihelcic, D., Müggen, P., et al. (2009). Intercomparison of Peroxy Radical Measurements Obtained at Atmospheric Conditions by Laser-Induced Fluorescence and Electron Spin Resonance Spectroscopy. *Atmos. Meas. Tech.* 2, 55–64. doi:10.5194/amt-2-55-2009

Fukui, K. (1981). The Path of Chemical Reactions - the IRC Approach. *Acc. Chem. Res.* 14, 363–368. doi:10.1021/ar00072a001

Gibb, E. L., Whittet, D. C. B., Boogert, A. C. A., and Tielens, A. G. G. M. (2004). Interstellar Ice: The Infrared Space Observatory Legacy. *Astrophys J. Suppl.* 151, 35–73. doi:10.1086/381182

**SUPPLEMENTARY MATERIAL**

The Supplementary Material for this article can be found online at: [https://www.frontiersin.org/articles/10.3389/fspas.2022.807649/full#supplementary-material](https://www.frontiersin.org/articles/10.3389/fspas.2022.807649/full#supplementary-material)

**Supplementary Figure S1** | Radial distribution functions (A) between the water oxygen in case of doped ice and pure ice at T=110K; (B) between the carbon atoms of the H2O and H2CO molecules.

**Supplementary Table S1** | Complete calculated reaction ER rate constants in cm3 molecule⁻¹ s⁻¹ for H2 formation on the grain model at CBS level.

**Supplementary Table S2** | Complete calculated reaction LH rate constants in s⁻¹ for H2 formation on the grain model at CBS level.

**Supplementary Table S3** | Calculated absolute energies (a.u.).
