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Determination of Core Losses Using an Inverse Modeling Technique

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ABSTRACT This paper presents an inverse thermal modeling technique to determine the core losses from the temperature rise inside the transformer core. For this purpose, initially, a customized printed circuit board (PCB) with thermal sensors is used to measure the temperature rise. Afterward, a 3D magneto-thermal forward model is developed to validate the temperature rise. The accuracy of the forward model is checked by comparing the simulated core losses and temperature rise of the transformer with experimental measurements for different supply conditions. The results show that the forward model can accurately estimate the core losses with a maximum relative error of less than 2.7% and predict the temperature rise in the core with a maximum relative error of less than 6.2%. Lastly, after ensuring the accuracy of the forward model, an inverse modeling technique is applied to the 3D thermal model to predict the core losses of the transformer directly from the measured temperature rise. The accuracy of the inverse model in estimating the core losses is checked by comparing the results with experimental measurements. The novel approach for the PCB design besides the inverse model shows that the technique can be applied to estimate the core losses directly from the measured temperature rise inside the core with a relative error of 2.7% compared to experiments.

INDEX TERMS Core losses, inverse modeling, loss model, temperature measurement, thermal model, thermal sensors.

I. INTRODUCTION

The increasing use of electrical machines in transportation and rapid industrialization has created the need for designing more efficient electrical machines. The strategy used by designers in developing more efficient machines is to reduce the generated losses, which can be classified into core losses, resistive losses, and mechanical losses. Hence, accurate prediction and measurements of these losses are essential for the evaluation of efficiency, temperature distribution, and cooling requirements of the electrical machine. Core losses are one of the most important parameters considered during the designing stage of electrical machines. Therefore, accurate estimation and reduction of core losses are vital to designing efficient electrical machines [1].

Several analytical and numerical models were widely used by machine designers to estimate the core losses in magnetic materials [2]–[6]. Separation models were used in [2]–[4] to estimate the core losses. With this method, the total core losses were obtained as the summation of the hysteresis loss, eddy-current loss, and excess loss. An empirical model based on Steinmetz equation was presented in [6] and [5] to estimate the core losses. Although these models present a fast way to estimate the core losses; however, they are based on constant coefficients that require several measurements and fitting to identify. Moreover, the coefficients change with the flux density, frequency, and type of material [7].

Another approach used for estimating power losses is based on inverse thermal models. The main theory is that power losses generated in the different parts of an electrical machine contribute directly to heat. Therefore, by measuring the temperature rise at any point in a machine, the losses can be inversely determined. This principle was applied in [8]–[12] to estimate the power losses and thermal parameters of electrical machine. Calorimetric method described in [9] and [11] was used to determine the losses directly from
the heat dissipation of the machine. Although a significant accuracy is reached with this method, the design and construction processes of the setup take a long time and can be unsuitable for industrial applications.

Using the lumped parameter thermal network (LPTN) in combination with the experimental measured temperature rise, the net power losses in an induction machine were segregated in [12] by inverse thermal method. This approach was used in [10], [13], and [14] to identify the thermal parameters used in the real-time prediction of stator and rotor temperature variations for condition monitoring of electrical machines. Nevertheless, LPTN involves approximation of geometry and thermal material properties of the machine in nodes. Hence, the reliability and the accuracy of such thermal network is strongly affected by the model designer. Alternatively, in [8], highly accurate results were obtained by using a finite-element model (FEM) to validate the temperature rise that was measured with built-in resistance temperature detectors inside the machine. However, the built-in sensors in the machine parts are prone to failures, and also placing the sensors in the interior parts of the machine is difficult.

In this paper, we present a method to estimate the core losses in a transformer from the measured temperature rise inside the core by inverse modeling technique. We introduce a customized sensor board consisting of thermal sensors to access the interior part of the transformer and minimize the measurement noise. Initially, a 3D magneto-thermal model for the transformer is developed in COMSOL-Multiphysics to validate the measured temperature rise. After modeling the temperature rise properly with the forward model, the core losses are then predicted from the presented inverse thermal model with high accuracy.

The remainder of this paper is organized as follows. In Section 2, the measurement system is described in detail. The models developed based on the experimental measurements are presented in Section 3. Afterward, the applications of the models and obtained results are presented in Section 4. Then, in Section 5, the most important findings of this study are summarized.

II. EXPERIMENTAL MEASUREMENTS

Experimental measurements of core losses and temperature rise are performed at different cases of supply voltages under the sinusoidal excitation with the fundamental frequencies between 50-150 Hz on a single-phase shell-type transformer under no-load conditions. The transformer core is cut from electrical steel sheets with a lamination thickness of 0.5 mm, and the material grade is M400-50A. Figure 1(a) shows the transformer under test with the power supply feeding it. NI USB-6251 data acquisition device (DAQ2) is used to retrieve the primary current \( i_1 \) and the induced voltage in the secondary side \( u_2 \) with respect to time. The core losses are computed from these measurements during the post-processing stage. The temperature rise of the transformer is measured with two thermal PCBs placed inside the transformer core, PT100 thermal sensors are embedded in the board as shown in Fig.1(b).

![Experimental measurement setup.](image)

**FIGURE 1.** (a) Experimental measurement setup. (b) Electronic board with PT100 temperature sensors.

A. LOSS MEASUREMENT

The total loss consist of core and copper losses. Sinusoidal voltage \( u_1 \) is supplied to the primary winding of the transformer at no-load. The primary current \( i_1 \) is obtained through the shunt resistor connected in series to the input terminal and the induced voltage in the secondary side \( u_2 \) is measured directly from the secondary winding of the transformer. The magnetic flux density \( B(t) \) in the middle limb section of the transformer is computed using (1).

\[
B(t) = \frac{1}{N_2 A_{lm}} \int u_2(t) dt,
\]

where \( N_2 \) is the number of turns in the secondary winding, and \( A_{lm} \) is the cross-sectional area of the middle limb. The magnetic field intensity \( H(t) \) at the lamination surface is calculated from the measured no-load current using (2).

\[
H(t) = \frac{N_1 i_1(t)}{l_{av}}
\]
where $N_1$ is the number of turns in the primary winding and $l_{av}$ is the mean length of flux path. The core loss density $p_{tot}$ is obtained from the integral of (1) and (2) over one supply period $T$ as given in (3).

$$p_{tot} = \frac{1}{T \rho} \int_0^T B(t)H(t)dt$$  \hspace{1cm} (3)$$

where, $\rho$ is the mass density of the core material. Using (4), the winding resistive losses $P_R$ is computed taking into account the effect of temperature rise on the winding resistance. Here, only the DC component of the resistive losses $P_R$ is considered.

$$P_R = I_{pri,rms}^2 R_{dc,pri}(1 + \alpha T)$$  \hspace{1cm} (4)$$

where, $R_{dc,pri}$ is the measured DC winding resistance, $\alpha$ is the thermal resistivity of copper, and $\Delta T$ is the change in temperature over the measurement duration.

**B. THERMAL MEASUREMENT**

The objective of the thermal measurement setup is to obtain temperature rise inside the transformer core and winding. For this purpose, two PCB boards with a thickness of 0.5 mm embedded with PT100 temperature sensors are used. The PCB is designed to perfectly match the geometry of the transformer core as shown in Fig. 1(b). Each board consists of 14 PT100 temperature sensors that are evenly placed over the geometry to accurately measure the temperature distribution of the transformer core during power switch ON. The sensors have a measurement range of $-50°C$ to $250°C$ and can measure the temperature rise of the transformer with an accuracy of $\pm 0.06°C$. An Agilent 34970A data acquisition unit (DAQ) is connected to the sensor board serial output port. The transformer temperature rise is recorded for 4 hours under no-load conditions. The measured temperature is used to estimate the core losses by applying the inverse modeling technique. The results obtained are compared with the measured core density in Section IV-D to test the accuracy of the loss identification approach.

**III. FORWARD MODELING**

This section describes the electromagnetic loss model and thermal model used for simulating the temperature rise of the transformer that occurs in the real situation. The models are developed with COMSOL-Multiphysics. The major dimensions and the parameters used in the model design are shown in Table 1. The flow chart of the modeling technique is shown in Fig. 2. In the following parts of this section, each step will be explained in detail.

**A. ELECTROMAGNETIC LOSS MODEL**

A 2D electromagnetic model of the transformer is implemented to achieve an accurate quantification of the distribution of the core losses, taking into account the realistic flux density distribution. The model assumes that the flux distribution is constant in the core thickness direction. The 2D model description of the transformer used in the simulation with the mesh is shown in Fig. 3(a). To predict the flux density and loss distribution in the transformer core, time-stepping magnetic field simulation is carried out by applying sinusoidal voltage $u_1$ to the input terminal of the primary winding at no-load as shown in Fig. 3(b).

![Figure 3](image-url)
distribution by using (5) during FEM post-processing.

\[ p_{\text{fe,(sim)}} = K_{\text{hys}} \sum_{i=1}^{N} f_i \cdot B_i^1 + K_{\text{eddy}} \sum_{i=1}^{N} f_i^2 \cdot B_i^2 + K_{\text{exc}} \sum_{i=1}^{N} f_i^{1.5} \cdot B_i^{1.5} \]  

(5)

where, \( N \) and \( f_i \) are the total number of harmonics and the frequency at each harmonic, \( K_{\text{hys}}, K_{\text{eddy}}, \) and \( K_{\text{exc}} \) are the hysteresis, eddy-current, and excess loss coefficients, respectively. These coefficients are obtained experimentally by fitting the coefficients of (5) to the measured core losses at different frequencies. Finally, the accuracy of the electromagnetic loss model is compared with the measured core losses. The comparisons are shown in the results section.

![Diagram of thermal model](image)

**FIGURE 4.** (a) 3D thermal model description. (b) Sensor location description in the core. Red marker indicates the sensors used in the measurements.

### B. THERMAL MODEL

The 3D thermal model described in Fig. 4(a) is used to analyze the temperature rise distribution of the transformer. The locations of the sensors used for the measurements of temperature rise are given in Fig. 4(b). The physics used in the modeling is based on the first law of thermodynamics and Fourier’s law. Mathematically, it can be expressed by the heat diffusion equation (6), which is the law governing heat transfer in electrical machines.

\[ \rho C_p \frac{\partial T}{\partial t} - \nabla \cdot (k \nabla T) = p_{\text{gen}} \]  

(6)

where, \( \rho, C_p, T, \) and \( p_{\text{gen}} = p_{\text{fe,(sim)}} \) are specific heat capacity, thermal conductivity, temperature, and heat source, respectively. The distribution of the core losses obtained in Section III-A and uniform loss density are coupled to the thermal model as the core heat source. The resistive loss obtained from (4) is used as the heat source in the primary winding region. To simplify the simulated geometry, homogenization approach used in [15] defined by (7) and (8) are applied to the specific heat capacity and mass density to account for the composite material properties. Due to the symmetry of the transformer, only half of the geometry is used in the simulation.

\[ C_p = \lambda_1 C_{p,1} + (1 - \lambda_1) C_{p,2} \]  

(7)

\[ \rho = \lambda_1 \rho_1 + (1 - \lambda_1) \rho_2 \]  

(8)

where, \( \lambda_1 \) is the filling factor of core/winding, \( C_{p,1} \) is the constituent specific heat capacity of core/winding, \( C_{p,2} \) is the constituent specific heat capacity of the insulation layer, \( \rho_1 \) is the mass density of core/winding, \( \rho_2 \) is the mass density of insulating material. The anisotropic property of the thermal conductivity of the core and winding are modeled in two directions by using (9) for the lapping direction and (10) for the transverse direction as in [15], which are expressed below:

\[ k_{lp} = \lambda_1 k_1 + (1 - \lambda_1) k_2 \]  

(9)

\[ k_{ts} = \frac{(1 + \lambda_1) k_1 + (1 - \lambda_1) k_2}{(1 - \lambda_1) k_1 + (1 + \lambda_1) k_2} \]  

(10)

Here, \( k_1 \) is the thermal conductivity of core/winding and \( k_2 \) is the thermal conductivity of insulating material. Newton’s law of cooling defined by (11) is assigned to the boundary surface as defined by (12)

\[ h = \frac{q}{A \sqrt{(T - T_{\text{ext}})}} \]  

(11)

\[ h = \begin{cases} h_1, & \text{on the winding surface} \\ h_2, & \text{on the core surface} \\ h_3, & \text{on the surface between the core and winding} \end{cases} \]  

(12)

where, \( q, T, T_{\text{ext}}, A, \) and \( h \) are the surface heat flux, temperature, surrounding temperature, surface area, and heat transfer coefficient, respectively. However, determining the heat transfer coefficient \( h \) can be quite challenging, as it depends on various factors such as surface temperature, ambient properties, and the nature of surfaces. Furthermore, it is determined in [16] that during natural cooling, about 25-30% of the heat flux is evacuated from the surface through radiation. Hence it is important to consider the effect of radiation on the total heat transfer coefficient. In this paper, the heat transfer coefficients are determined analytically by using (13)

\[ h = h_{\text{conv}} + h_{\text{rad}} \]  

(13)

Here \( h_{\text{conv}} \) and \( h_{\text{rad}} \) are natural convection and radiation coefficients. The natural convection coefficient \( h_{\text{conv}} \) is calculated from the Nusselt number \( Nu \) similar to [17], which is given by (14) and the radiation coefficient is estimated by using (15) [18],

\[ h_{\text{conv}} = \frac{Nu \cdot k_{\text{flhd}}}{L_c} \]  

(14)

\[ h_{\text{rad}} = \epsilon \cdot \sigma \cdot \left( T^2 - T_{\text{ext}}^2 \right) \cdot (T - T_{\text{ext}}) \]  

(15)

where \( k_{\text{flhd}} \) is the fluid thermal conductivity, \( \sigma \) is the Stefan-Boltzmann constant, \( L_c \) is the characteristic length and \( \epsilon \) emissivity of the cooling surfaces. The convective heat coefficient is calculated for each of the surfaces. The equivalent heat transfer coefficient \( h \) of the composite surface is estimated by using the area-based composite correlation given in (16),

\[ h = \frac{h_1 A_1 + h_2 A_2 + \ldots}{A_T} \]  

(16)
where \( A_T, h_1, h_2 \ldots \) and \( A_1, A_2 \ldots \) are the total surface area, heat transfer coefficients, and surface area of each surface considered, respectively. Figure 5 shows the plot of the convective coefficient of the transformer for different temperature gradients by considering the radiation effect on the boundary surfaces.

\[
\begin{align*}
A_T, & 
\quad \text{total surface area}, \\
h_1, h_2 \ldots & 
\quad \text{heat transfer coefficients}, \\
A_1, A_2 \ldots & 
\quad \text{surface area of each surface considered}.
\end{align*}
\]

Figure 5 shows the plot of the convective coefficient of the transformer for different temperature gradients by considering the radiation effect on the boundary surfaces.

**IV. APPLICATIONS AND RESULTS**

**A. IDENTIFICATION OF LOSS COEFFICIENTS**

Experimental measurements are carried out at sinusoidal excitation of different frequencies to estimate the loss coefficients. The flux density and core loss density are calculated from the measured no-load current \( i_1 \) and open-circuit voltage \( u_2 \) (see Fig. 1(a)) by using (1)-(3). The core loss coefficients are obtained by fitting Bertotti’s formula (5) against the measured core loss density by using the flux density data at different excitation levels and frequencies in the range of 10 Hz - 150 Hz. Figure 6 shows the measured core losses and estimated core losses by using the fitted coefficients. The maximum relative fitting error of the coefficients is 5%.

**B. ELECTROMAGNETIC MODEL LOSS CALCULATION**

Consequently, a time-varying magnetic field simulation is performed by applying a sinusoidal voltage to the primary winding of the magnetic model. Figure 7(a) shows the simulated flux density distribution of the 2D model. Fast Fourier Transform (FFT) is performed on the flux density distribution of each element to obtain the harmonic components of the flux density due to the non-linearity of the core material. The related core loss density distribution of the machine shown in Fig. 7(b) is calculated by using (5) from the identified loss coefficients. The simulated losses are compared with the measurements in Table 2 to validate the accuracy of the magnetic loss model.

**TABLE 2.** Comparison of the core losses at different frequencies.

| \( f \) (Hz) | Core loss density (W/kg) | Measured | Simulated | Relative error (%) |
|-------------|--------------------------|----------|-----------|-------------------|
| 10          | 0.38                     | 0.39     | 2.63      |                   |
| 25          | 1.20                     | 1.21     | 0.83      |                   |
| 50          | 3.04                     | 3.05     | 0.33      |                   |
| 100         | 8.66                     | 8.64     | 0.23      |                   |
| 150         | 16.78                    | 16.77    | 0.06      |                   |

The comparison shows that the magnetic model can accurately predict the losses at different frequencies. Hence, the results obtained can be used in the forward model to predict the temperature rise of the transformer.

**C. THERMAL MODEL SIMULATIONS**

Firstly, the core loss density distribution obtained from the 2D magnetic loss model and the winding loss obtained from (4) is inputted to the core and primary winding as a heat source of the thermal model as shown in Fig. 8(a). Next, the heat...
source of the core region is replaced with uniform loss density obtained from the average core loss density of the magnetic loss model and the winding heat source remains constant as shown in Fig. 8(b). The model is simulated for 4 hours in both cases to obtain the temperature distribution shown in Fig. 9.

From Fig. 9, it can be observed that the temperature distribution is uniform in the transformer core region for the simulated cases. However, temperature variation is observed in the winding geometry. This is because the variation of losses inside the core and edges are insignificant with respect to the overall volume of the transformer core. Furthermore, the accuracy of the forward thermal model to simulate the transformer temperature rise distribution under different supply conditions is tested by comparing (Fig. 10) the simulated temperature rise with the measured temperature rise iteratively over time until the best fit for the predicted core loss density $p_{tot,(prd)}$ is obtained. The routine is repeated for the different measurement cases and the results obtained are compared with the measured core loss density in Table 4.

### Table 3. Forward model relative error comparison for different sensors located inside the core at steady-state condition. Core heat source: distributed loss (DL) and uniform loss (UL).

| $f$ (Hz) | P1 | P2 | P3 | P4 | P5 | P6 | P7 | P8 | P9 | P10 |
|----------|----|----|----|----|----|----|----|----|----|-----|
| 50 (DL)  | 1.84 | 2.42 | 3.71 | 2.52 | 5.34 | 1.92 | 2.63 | 3.02 | 1.33 | 4.38 |
| 50 (UL)  | 2.49 | 3.07 | 4.37 | 3.18 | 6.14 | 2.62 | 3.43 | 3.74 | 2.11 | 5.40 |
| 100 (DL) | 1.37 | 1.45 | 1.87 | 2.66 | 1.61 | 1.74 | 2.94 | 1.73 | 3.33 | 0.79 |
| 100 (UL) | 1.02 | 1.10 | 1.49 | 2.48 | 1.12 | 1.32 | 1.92 | 1.28 | 2.80 | 0.04 |
| 150 (DL) | 0.23 | 0.15 | 0.77 | 0.31 | 0.67 | 0.03 | 0.47 | 1.10 | 0.63 | 2.22 |
| 150 (UL) | 0.22 | 0.35 | 1.00 | 0.08 | 1.03 | 0.25 | 0.08 | 1.40 | 0.23 | 2.89 |

### Table 4. Core loss density comparison at different frequencies.

| $f$ (Hz) | Measured | Predicted | Relative error (%) |
|----------|----------|-----------|-------------------|
| 50       | 3.64     | 2.96      | 2.63              |
| 100      | 8.66     | 8.75      | 1.04              |
| 150      | 16.78    | 16.62     | 0.95              |

The results show that the inverse model accurately predicts the core loss density from the measured temperature inside the transformer core with a maximum difference of less than 2.7%. The results returned from the inverse model are unique for each measured case. In other words, each time the inverse model is run for the same case, a unique solution is obtained in terms of the core loss density. The predicted temperature rise for the obtained core loss density $P_{tot,(prd)}$ from the inverse model is compared against the measured temperature rise for different sensor locations P1, P4, P5, and the winding as shown in Fig. 12.

Figure 12 shows that the predicted temperature rise matches reasonably well against the measurement results.
A detailed comparison of the predicted temperature rise for each sensor located inside the core with the measured temperature rise is given in Table 5.

The comparison in Table 5 shows that the inverse model accurately predicts the steady-state temperature rise distribution of the transformer with a relative error of less than 3.6% for all cases. However, when considering complex core geometry like the stator core of an induction machine, the basic assumption of a uniform heat source might increase the error in predicting the core losses because of the clear distinction of the yoke and teeth loss density. Therefore, defining a distributed heat source in the core and using the measured temperature rise for the different locations in the stator core will improve the accuracy of the inverse model results.
V. CONCLUSION
In this paper, we presented an inverse modeling technique to estimate the core losses of a transformer operating at no-load based on the measured temperature rise and its numerical thermal model. With the use of the customized sensor board, the method ensures the reliability of the temperature rise measurements, which is vital for the inverse modeling approaches. The proposed method can be applied on any electrical machine irrespective of the geometry with the appropriate design of the sensor board, which can be useful for condition monitoring and fault diagnosis purposes.

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