Anisotropic resonance modes emerging in an antiferromagnetic superconducting state

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Two strong arguments in favor of magnetically driven unconventional superconductivity arise from the coexistence and closeness of superconducting and magnetically ordered phases on the one hand, and from the emergence of magnetic spin-resonance modes at the superconducting transition on the other hand. Combining these two arguments one may ask about the nature of superconducting spin-resonance modes occurring in an antiferromagnetic state. This problem can be studied in underdoped BaFe2As2, for which the local coexistence of large moment antiferromagnetism and superconductivity is well established by local probes. However, polarized neutron scattering experiments are required to identify the nature of the resonance modes. In the normal state of Co underdoped BaFe2As2 the antiferromagnetic order results in broad magnetic gaps opening in all three spin directions that are reminiscent of the magnetic response in the parent compound. In the superconducting state two distinct anisotropic resonance excitations emerge, but in contrast to numerous studies on optimum and over-doped BaFe2As2 there is no isotropic resonance excitation. The two anisotropic resonance modes appearing within the antiferromagnetic phase are attributed to a band selective superconducting state, in which longitudinal magnetic excitations are gapped by antiferromagnetic order with sizable moment.

The emergence of spin-resonance modes (SRM) in several superconductors is interpreted as key evidence for unconventional pairing mediated through magnetic fluctuations1. The resonance mode can be explained as a spin excitation, which requires a sign change of the superconducting (SC) gap. Neglecting spin-orbit coupling the SRM is expected to be isotropic in spin space, while for dominant spin-orbit coupling an Ising-type resonance mode arises, as it was indeed observed in the 4f compound CeCoIn52. In Fe-based superconductors3–6 the multi-band multi-orbital Fermi surface combined with medium-sized spin-orbit interaction results in a complex interplay. That spin-orbit coupling is non-negligible in Fe-based superconductors can be learned from the large anisotropy gaps in the magnon dispersion in the antiferromagnetic (AFM) parent materials7. In pure BaFe2As2, the in-plane anisotropy is even larger than the out-of-plane one3, which points to a lifting of the tetragonal orbital degeneracy. Signatures of qualitatively the same spin-space anisotropy have been observed in the superconducting states in several FeAs-based superconductors. Polarized inelastic neutron scattering (INS) experiments on optimum Co-doped BaFe2As2 show that two distinct resonance components appear at the SC transition, of which the lower one is anisotropic3 while a broader mode at larger energy remains isotropic. Similar experiments on Ni7 and K-optimum-doped BaFe2As210 have established qualitatively the same double resonance excitations as a general property of doped BaFe2As2. Furthermore, even in K-overdoped BaFe2As2 an anisotropic additional low-energy SRM remains visible ruling out that it just arises from the presence of quasi-static magnetic order. In Co-doped NaFeAs14,15 and in Na-doped BaFe2As2 the low-energy features even dominate the magnetic scattering in the SC state while there is only an anisotropic shoulder. For optimum- and over-doped BaFe2As2 the spin-space anisotropy of the lower SRM corresponds to the two magnetic soft axes of pure BaFe2As2. These are along the in-plane component of the propagation vector4–6, along which moments align ([110] direction in the tetragonal lattice and [001] in the orthorhombic notation), and along c.
In contrast the orthorhombic $b$ direction forms the hard magnetic axis with the large anisotropy gap in the magnetic dispersion. This picture of two magnetically soft directions is nicely corroborated by the recent observation of the spin-reorientation transition in Na-doped BaFe$_2$As$_2$, which leads to an AFM ordered moment along the $c$ direction.

Various models were proposed to explain the coexistence of anisotropic and isotropic resonance features. The low-energy resonance has been ascribed to quasi-static correlations while the isotropic resonance at higher energy is explained by the usual triplet exciton. In another approach the split resonance is attributed to an orbital and band selective pairing, which retains some well-defined orbital character in the low-energy resonance modes.

So far, polarized INS experiments on the spin-space anisotropy were performed only for near to optimum, or overdoped BaFe$_2$As$_2$ with strongly suppressed AFM correlations (ordered moment of less than 5% of that in the pure material). Therefore, no sizable spin gap arising from the antiferromagnetic order can be expected, while the SC gaps are large. However, the phase diagram of Co-doped BaFe$_2$As$_2$ offers the rather unique possibility to study the emergence of SRMs in a robust AFM state, which has not been fully explored in any of the unconventional superconductors.

In this work we study 4.5% Co underdoped BaFe$_2$As$_2$ that exhibits microscopic coexistence of SC and AFM order, see Fig. 1, with an ordered magnetic moment of about 20% of that in the parent compound. Many unpolarized INS studies on almost the same concentration were reported, revealing the appearance of a broad resonance feature near 4.5 meV, but only the polarized experiments presented here can show that the character of resonance modes in this AFM phase is fundamentally different from that at optimum or higher doping.

### Results

Throughout this paper we use the tetragonal notation and performed all experiments in the [110]/[001] scattering plane. For the polarization analysis the frame of reference is defined as $x$ parallel to the scattering vector $Q$ (here all magnetic scattering contributes to the spin flip (SF)$_x$ channel), $z$ perpendicular to the scattering plane, and $y$ perpendicular to $x$ and $z$. This allows us to extract the contributions along the three directions in spin-space with respect to the ordered moment: longitudinal, $t_{\text{long}} \equiv a_{\text{orth}}$, transverse in-layer, $t_{\text{out}} \equiv b_{\text{orth}}$, and transverse out-of-layer, $t_{\text{out-c}}$, see Fig. 2a.

Figure 1 resumes the various transitions appearing in Ba(Fe$_{0.955}$Co$_{0.045}$)$_2$As$_2$. The emergence of orthorhombic domains results in a lower crystal quality, and thus in a reduced extinction effect and enhanced Bragg intensity. Therefore, no sizable spin gap arising from the antiferromagnetic order can be expected, while the SC gaps are large. However, the phase diagram of Co-doped BaFe$_2$As$_2$ offers the rather unique possibility to study the emergence of SRMs in a robust AFM state, which has not been fully explored in any of the unconventional superconductors.

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![Figure 1](https://www.nature.com/scientificreports/)
Figure 2. Magnetic fluctuation spectra in the AFM and SC states at various $l$ values. (a) Sketch of the three orthogonal directions with respect to the ordered Fe moment. (b) Geometrical conditions for polarized INS at $(0.5, 0.5, l)$ with respect to the spin-space anisotropy. (c–e) Polarized INS intensity at $(0.5, 0.5, l)$ with $l = 1, 3$ and 5 in the different spin-flip (SF) channels after subtracting the background and correcting for the Bose and form factors. These data correspond to the dynamical susceptibilities $\chi''$ multiplied with the geometry factors and folded with resolution function. The nine curves are consistently fitted (lines) by the three susceptibilities $\chi''_\text{long}$, $\chi''_\text{t-in}$ and $\chi''_\text{t-out}$ each described by a single log-normal distribution. These individual susceptibilities are resumed in (f); their amplitude follows an $1/E$ relation. A fit with a single relaxor function is not possible, as indicated by the dotted line in (c). (g–i) The same data in the SC phase at 1.5 K, where only two additional resonance components in $\chi''_\text{t-in}$ and $\chi''_\text{t-out}$ are needed to again consistently describe all nine curves. These additional resonance contributions are shown in (j), where dashed lines denote the anisotropic response in the normal state (same as in (f)).
long direction, that appear in SFz. The SC transition at 14 K, determined through neutron polarization (see Methods and Fig. 1(a)), also leads to suppression of the magnetic intensity at the (0.5,0.5,3) magnetic Bragg peak by about 26% and to an increase of inelastic scattering at (0.5,0.5,1) and 5 meV, which corresponds to appearance of the resonance mode, see Fig. 1(b), and the discussion below. All transition temperatures, the suppression of AFM moment at \(T_c\) and the emergence of SRMs perfectly agree with the literature4–6,21.

By the aid of neutron-polarization analysis we are able to separate the magnetic fluctuations according to the three directions. Polarized INS scans at (0.5,0.5,0,5) with \(l = 1, 3\) and 5 are shown in Fig. 2. These \(Q\) vectors correspond to AFM zone centers and the variation of the \(l\) values allows one to separate the long and \(t \rightarrow o\) directions through the geometry factor \(\sin^2(c)\), see Methods. For small \(l\) the \(c\) or \(t \rightarrow o\) direction is almost perpendicular to \(Q\), so that the SFz signal essentially corresponds to the \(t \rightarrow o\) direction. In contrast, at large \(Q\) \(Q\) is nearly parallel to \(c\), so that the SFz channel essentially contains the long direction. The \(t \rightarrow in\) contribution exclusively contributes to the SFy channel with full geometry factor. The difference SFy + SFz-SFx gives a direct determination of the background, and 2SFz-SFy-SFz gives the total magnetic scattering besides the correction for finite flipping ratios. Figure 2c–e shows the signal in the SF channels after subtracting the background. (The magnetic response also enters the SFy and SFz channels and can be obtained by SFy-SFx and SFz-SFx, and these data yield a fully consistent result, that, however, suffers from much lower statistics due to the larger SFy background). The data were corrected for higher-order contaminations of the monitor, the Bose factor and for the form-factor, so that they correspond to the imaginary part of the susceptibilities multiplied with the geometry factors, \(\sin^2(c)\), described above. The nine spectra can be consistently described by the three susceptibilities \(\chi'^long\), \(\chi''t \rightarrow in\) and \(\chi''t \rightarrow out\). Each of these is well described by a log-normal distribution, \(A \exp \left(-\frac{(2\ln E - b \ln t)^2}{2\sigma^2}\right)\), which fits all spectra with only three parameters. In contrast to this satisfactory description, the magnetic spectra below \(T_N\) cannot be fitted by the relaxor function, \(A \frac{E - t}{E + t}\). The asymmetric spectral shape resulting from the instrumental resolution and from disorder-induced broadening is well captured by the log-normal distribution. By a concomitant fit of all spectra we obtain the three susceptibilities shown in Fig. 2f. The magnetic response of Ba(Fe0.955 Co0.045)2 As2 can be well understood as the spin-wave-like response of a magnetically ordered material with disorder 7, 21. In the transversal channels \(t \rightarrow in\) and \(t \rightarrow out\), the well-defined spin gaps of the pure material at 18.9 and 11.6 meV are renormalized to broad maxima at 13.9 and 7.0 meV. Also in the long channel we find a gap at \(\sim16\) meV. In view of the report of a longitudinal gap in pure BaFe2 As2 of only 24 meV28, this would indicate a surprisingly small renormalization by 4.5% Co doping. In addition the strength of the longitudinal signal is comparable to that of the two transversal directions in the underdoped material, while much smaller longitudinal weight is reported in the pure crystal28. This sheds further doubts on the interpretation of the very weak signal in pure BaFe2 As2 as the longitudinal mode and supports an alternative two-magnon explanation29. By choosing the scattering vector \((0.5, 0.5, 0.5)\) in our sample crystal we select a single domain orientation for which the scattering vector constitutes a magnetic zone center, while it is a zone boundary for the other domain. Due to the very high magnon energies of the order of 200 meV, expected at the zone boundary, we may exclude any scattering from the other domain, as it has recently been proven in an experiment on a detwinned crystal31.

In Fig. 2g–i we present the same analysis of the magnetic scattering in the SC state. We can describe the nine spectra at the three studied scattering vectors by adding two resonance features, one in \(\chi''t \rightarrow out\) and one in \(\chi''t \rightarrow in\), to the fixed normal state susceptibilities determined at 15 K. That there are indeed two distinct resonance modes can be further seen in the SFy and SFz channels shown in Fig. 3a,b, respectively. The SFy only senses the \(\chi''t \rightarrow in\) with full geometry factor; therefore, we summed the data taken at the different \(l\) values. This \(\chi''t \rightarrow in\) resonance peaks at 5.9 meV. In contrast, \(\chi''t \rightarrow out\) and \(\chi''long\) contribute to the SFz channel with varying geometry factors (that always sum to one), see Fig. 2b. However, the \(\chi''long\) remains fully suppressed at energies below \(\sim8\) meV, therefore the additional resonance signal in the SFz channels always stems from \(\chi''t \rightarrow out\) and it peaks at 4.7 meV. The two resonance energies were obtained by a simultaneous fit of the spectra for \(l = 1, 3,\) and 5, at 1.5 K, see Fig. 2g–i by keeping the log-normal parameters identical to those determined at 15 K. Summing up all magnetic scattering at the three \(l\) values fully agrees with the unpolarized data taken previously25–28. Our analysis can be corroborated by fitting the \(l\) dependence of the magnetic signals shown in Fig. 4. A larger \(l\) favors the observation of \(\chi''long\) on the dispense of \(\chi''t \rightarrow out\) in the SFz channel. Therefore, we may determine the ratio \(p\) of the long component defined as \(p = \chi'^long / \chi'^t \rightarrow out\). At \(T = 58\) K above the Néel temperature all signals yield \(p = 0.5\) within the error bars, therefore there is no anisotropy between the two magnetically soft axes \(long\) and \(t \rightarrow out\), but the spectral weight along \(t \rightarrow in\) (contributing to SFy) remains suppressed. The critical scattering of the AFM transition thus appears predominantly in the two soft directions, and small low-energy anisotropy remains even visible above \(T_\chi\) at 70 K. However, at 15 K in the AFM phase and at 1.5 K in the SC and AFM phase we find an insignificant \(long\) component in the SFz channel, \(p \sim 0\), in agreement with the conclusion that longitudinal excitations are gapped due to the significant ordered moment, see Fig. 4c–h. The same \(l\) analysis for the additional low-energy resonance signal in optimum-Co-doped BaFe2 As2 (\(x = 0.06\)) is shown in Fig. 4a. The slow reduction of the SFz signal with \(l\) indicates that there is a significant, \(p = 0.28\), longitudinal component in this low-energy resonance mode at optimum doping; similar results were reported for optimum Ni doped3 and K overdoped30 BaFe2 As2.

Discussion

The anisotropy of the resonance excitations in underdoped Ba(Fe0.955 Co0.045)2 As2 is fundamentally different from that seen in the near-optimum or overdoped BaFe2 As2 crystals studied previously by polarized INS experiments. This excludes a recently proposed generic explanation of the double resonance27. There is no isotropic SRM in the underdoped material, which can be associated with the usual spin triplet excitation1. Instead there are two polarized resonance modes appearing in the \(\chi''t \rightarrow out\) and \(\chi''t \rightarrow in\) Channels. The reason for these fully anisotropic resonances...
seems to consist in the gap that opens in $\chi''_{\text{long}}$ due to the AFM ordering. Although this longitudinal gap is renormalized from the expected one in pure BaFe$_2$As$_2$ (considering the optical studies$^{32,33}$) it is still considerably larger than twice the SC gap $2\Delta\sim8$ meV determined in ARPES experiments$^{27}$. Therefore, longitudinal fluctuations cannot interplay with the superconductivity in this underdoped material, and they cannot contribute to a lowering of exchange energy$^1$. This yields a simple explanation for the reduced SC transition temperature although the high-energy longitudinal fluctuations still contribute to the pairing. The fact that we do not see longitudinal excitations in the SC state in contrast to the optimum or overdoped samples, furthermore, confirms that superconductivity and AFM ordering coexist locally for 4.5% Co-doping as it was reported by NMR and $\mu$SR studies$^{19,20}$.

The anisotropic magnetic excitations are qualitatively compared in Table 1. At large temperatures the magnetic response is well described by a nearly isotropic relaxor behavior, which turns more and more anisotropic upon approaching the AFM and SC transitions in the underdoped and optimally doped compounds, respectively. Such an anisotropic relaxor response upon approaching a magnetic instability can be easily explained in random phase approximation, and has also been reported in Sr$_2$RuO$_4$, which is close to a incommensurate magnetic ordering but not reaching it$^{34}$. In both Co-doped compounds the softer relaxor functions are observed along the two soft magnetic axes. Entering the SC state directly (optimum doping) or through the AFM phase (underdoping) results, however, in different behaviors. For optimum doping the two soft magnetic directions of the normal state constitute the low-energy anisotropic SRM, while a second SRM at larger energy remains isotropic$^8$–$^{11}$. In contrast, in the underdoped state the spin gaps induced by the AFM order dominate and result in SRMs appearing only in the two transverse channels. There is no isotropic SRM and the longitudinal channel does not contribute at all to SRMs in the AFM superconductor. Fundamentally different SRMs thus emerge in the under- and optimally doped samples as a result from the different phases from which SC emerges. A full explanation of the anisotropic SRMs thus needs to take the multi-orbital and multi-band structure into account as well as the selective SC pairing arising therein.

The emergence of SC in the AFM state of Ba(Fe$_{0.955}$Co$_{0.045}$)$_2$As$_2$ bears some resemblance to SC appearing in Fe-based compounds, in which the hole Fermi surfaces at the zone center are suppressed; nevertheless SC can be explained by spin fluctuations in such case$^{15}$. The anisotropic spin–resonance modes emerging in the antiferromagnetic and superconducting phase of Co-underdoped BaFe$_2$As$_2$ reveal the high complexity of its superconducting state. While in the case of a conventional multi-band superconductor, such as MgB$_2$, different gaps develop on distinct bands, the addition of spin–orbit coupling and the coexistence of magnetic order put much higher constraints on the theoretical description of the superconducting state and mechanism. This physics is, however, not limited to the Fe-based superconductors, but is also relevant for various 4$f$ and 5$f$ systems, where the understanding of the electronic band structure seems less advanced. The spin-dependent band-structure of the antiferromagnetically ordered phase must form the theoretical basis, out of which the superconducting phase forms, but so far this band structure seems insufficiently known. Including spin–orbit coupling to the theory is also necessary, as otherwise the antiferromagnetic ordering would not open a gap in the transversal excitations. The strong gap in the longitudinal magnetic excitations arising from the AFM order is remarkable and prevents any coupling with superconductivity.

![Figure 3. Emergence of two anisotropic spin resonance modes below $T_C$. (a) SFz scattering at different $l$ values with the analysis of Fig. 1b. Comparison of SFy intensities obtained above and below $T_C$ since this channel only contains $\chi''_{\text{t-out}}$, the results obtained at $l=1$, $3$ and $5$ were added and lines correspond to the analysis presented in Fig. 1. The intensity enhancements in the SFz (c) and SFy (d) channels clearly peak at different energies indicating the different SRMs at 4.7 meV ($\chi''_{\text{t-out}}$) and 5.9 meV ($\chi''_{\text{t-in}}$).](#)
This effect might give a clue to the superconducting mechanism, because the \( T_c \) is strongly reduced compared to the maximum value of 24 K appearing at only slightly higher doping.

**Figure 4.** Polarization of resonance signals in 6% and in 4.5% Co-doped BaFe\(_2\)As\(_2\). \( l \) dependence of the scattering in various SF channels which allows one to separate the \( \chi''_{\text{long}} \) and \( \chi''_{\text{t-out}} \) components in the SFz channel. The parameter \( p \) describes the contribution of \( \chi''_{\text{t-out}} \) required to fit the \( l \) dependence. Panel (a) shows the low temperature results for the 4 meV signal in optimum doped Ba(Fe\(_{0.94}\)Co\(_{0.06}\))\(_2\)As\(_2\), which has no \( t-in \) component but consists of 29% of \( \text{long} \) signal. In contrast, the isotropic resonance at \( \sim 8 \) meV appears equally strong, \( p = 0.5 \), in the three directions (b). Panels (c–k) present the same analysis in Ba(Fe\(_{0.955}\)Co\(_{0.045}\))\(_2\)As\(_2\) for energies of 3, 5 and 7.5 meV, when not labelled differently, at \( T = 1.5 \) K in the SC state, at 15 K in the non-SC AFM phase, and at 58 K in the paramagnetic phase.
In summary polarized INS experiments on the magnetic response in underdoped AFM Ba(Fe_{0.95}Co_{0.05})_2As_2 reveals a fundamentally different behavior compared to previously studied compounds with a larger amount of doping. The significant ordered moment results in sizable spin gaps opening in the magnetic excitations along all three directions. Longitudinal fluctuations remain unaffected by the SC transition, because the corresponding AFM spin gap clearly exceeds twice the SC one. In the SC state two resonance components can be separated that are both anisotropic in spin space, one appearing in $\chi'_{t-out}$, the other in $\chi'_{t-in}$. In contrast the anisotropic low-energy SRM at optimum doping appears in the $long$ and $t-out$ directions. The consistent description of the anisotropic SRMs appearing in under- and optimally doped BaFe x As y certainly requires to take the detailed band- and orbital selective aspects of the SC pairing into account.

### Methods

Three single crystals of Ba(Fe_{0.95}Co_{0.05})_2As_2 were grown by the FeAs-flux method yielding a combined mass of 2.12 g co-aligned for the experiment. The 6% Co-doped sample used for comparison is the same as that studied in ref. 8.

Polarized INS experiments were performed on the IN20 and IN22 thermal triple axis spectrometers at the Institut Laue-Langevin in Grenoble. Both spectrometers were operated with Heusler monochromator and analyzer crystals, and a graphite filter was set between the sample and the analyzer in order to suppress higher order contaminations. Most data was taken with the final wave vector of the neutron fixed to 2.662 Å$^{-1}$. Experiments were performed with either the CRYOPAD device to assure zero magnetic field at the sample position or with Helmholtz coils to guide the neutron polarization at the sample. With the Helmholtz coils the guide field was not varied in the SC state in order not to deteriorate the neutron polarization (except for the $T_c$ measurement shown in Fig. 1b). The flipping ratio measured on nuclear Bragg peaks in the SC phase amounted to 14 on IN20 and 16 on IN22. Polarized INS allows one to separate magnetic and nuclear contributions and to split magnetic scattering according to the polarization direction of the magnetic signal. In general INS only senses magnetic signals that are polarized perpendicular to the scattering vector $Q$ resulting in a geometry factor $\sin^2(\alpha)$ with $\alpha$ the angle between $Q$ and the magnetic signal. With the longitudinal polarization analysis this active part of the magnetic correlations further splits. In the neutron spin-flip (SF) channel one finds the part that is also perpendicular to the neutron polarization direction, while the neutron non-spin-flip (NSF) channel contains the parallel polarization.

Varying the neutron-polarization guide fields in the SC state induces neutron depolarization, because the magnetic flux inside the sample is pinned. This depolarization induces a strong SF intensity on a non-magnetic Bragg peak. By following this erroneous intensity upon heating, the SC $T_c = 14$ K of the sample crystal is determined through the sharp drop of the spin-flip intensity associated with the depinning of guide fields and restoration of neutron polarization at $T_c$, see Fig. 1b.

### References

1. Scalapino, D. J. A common thread: The pairing interaction for unconventional superconductors. Rev. Mod. Phys. 84, 1383 (2012).
2. Raymond, S. & Lapertot, G. Ising Incommensurate Spin Resonance of CeCoIn 5: A Dynamical Precursor of the Magnetic Phase. Adv. Phys. 59, 803 (2010).
3. Kamihara, Y., Watanabe, T., Hirano, M. & Hosono, H. Iron-Based Layered Superconductor La[O1-xF x]FeAs (x = 0.05-0.12) with $T_c = 26$ K. J. Am. Chem. Soc. 130, 3296 (2008).
4. Johnston, D. C. The puzzle of high temperature superconductivity in layered iron pnictides and chalcogenides. Adv. Phys. 59, 803 (2010).
5. Hirschfeld, P. J., Korshunov, M. M. & Mazin, I. I. Gap symmetry and structure of Fe-based superconductors. Rep. Prog. Phys. 74, 124508 (2011).
6. Dai, P. Antiferromagnetic order and spin dynamics in iron-based superconductors. Rev. Mod. Phys. 87, 855 (2015).
7. Qureshi, N. et al. Local magnetic anisotropy in BaFe 2 As 2: A polarized inelastic neutron scattering study. Phys. Rev. B 86, 064010(R) (2012).
8. Qureshi, N. et al. Splitting of Resonance Excitations in Nearly Optimally Doped Ba(Fe_{0.94}Co_{0.06})_2As_2: An Inelastic Neutron Scattering Study with Polarization Analysis. Phys. Rev. Lett. 110, 137001 (2013).
9. Luo, H. et al. Spin Excitation Anisotropy as a Probe of Orbital Ordering in the Paramagnetic Tetragonal Phase of Superconducting BaFe 1.98Ni 0.02As 2. Phys. Rev. Lett. 111, 107006 (2013).
10. Zhang, C. et al. Magnetic anisotropy in hole-doped superconducting Ba$_{1-x}$K$_x$Fe$_2$As$_2$ probed by polarized inelastic neutron scattering. Phys. Rev. B 87, 081101(R) (2013).
11. Qureshi, N. et al. Anisotropy of incommensurate magnetic excitations in slightly overdoped Ba$_{0.8}$K$_{0.2}$Fe$_3$As$_2$ probed by polarized inelastic neutron scattering experiments. Phys. Rev. B 90, 100502 (2014).

| Superconducting | Normal state $T_c < T$ |
|-----------------|------------------------|
| 4.5% Under doped | $4.7$ meV $t-out$ $T_c < T_c$ glued $T_c \leq T$ anisotropic relaxor $T_c \ll T$ isotropic relaxor |
| 5.9 meV $t-in$ |
| 6% Optimum doped | $4$ meV $28\%$ long $T_c \ll T$ anisotropic relaxor $T_c \ll T$ isotropic relaxor |
| $9$ meV $isinotropic$ |
12. Zhang, C. et al. Anisotropic neutron spin resonance in underdoped superconducting NaFe$_{1-x}$Co$_x$As. Phys. Rev. B 90, 140502(R) (2014).
13. Zhang, C. et al. Measurement of a Double Neutron-Spin Resonance and an Anisotropic Energy Gap for Underdoped Superconducting NaFe$_{0.985}$Co$_{0.015}$As Using Inelastic Neutron Scattering. Phys. Rev. Lett. 111, 207002 (2013).
14. Walter, F. et al. Spin reorientation in Ba$_{1-x}$Na$_x$Fe$_2$As$_2$ studied by single-crystal neutron diffraction. Phys. Rev. B 91, 060505 (2015).
15. Qureshi, N. et al. Fine structure of the incommensurate antiferromagnetic fluctuations in single-crystalline LiFeAs studied by inelastic neutron scattering. Phys. Rev. B 90, 144503 (2014).
16. Knolle, J., Eremin, I., Schmalian, J. & Moessner, R. Magnetic resonance from the interplay of frustration and superconductivity. Phys. Rev. B 84, 180510(R) (2011).
17. Lv, W., Moreo, A. & Dagotto, E. Double magnetic resonance and spin anisotropy in Fe-based superconductors due to static and fluctuating antiferromagnetic orders. Phys. Rev. B 89, 104510 (2014).
18. Yu, R., Zhu, J.-X. & Si, Q. Orbital-selective superconductivity, gap anisotropy, and spin resonance excitations in a multiorbital t − J$_1$ − J$_2$ model for iron pnictides. Phys. Rev. B 89, 024509 (2014).
19. Laplace, Y., Bobroff, J., Ruiller-Albenque, F., Colson, D. & Forget, A. Atomic coexistence of superconductivity and incommensurate magnetic order in the pnictide Ba(Fe$_{1-x}$Co$_x$)$_2$As$_2$. Phys. Rev. B 80, 140501 (2009).
20. Marsik, F. et al. Coexistence and Competition of Magnetism and Superconductivity on the Nanometer Scale in Underdoped BaFe$_{1.89}$Co$_{0.11}$As$_2$. Phys. Rev. Lett. 105, 057001 (2010).
21. Pratt, D. K. et al. Coexistence of Competing Antiferromagnetic and Superconducting Phases in the Underdoped Ba(Fe$_{0.955}$Co$_{0.047}$)$_2$As$_2$ Compound Using X-ray and Neutron Scattering Techniques. Phys. Rev. Lett. 103, 087001 (2009).
22. Julien, M.-H. et al. Homogeneous vs. inhomogeneous coexistence of magnetic order and superconductivity probed by NMR in Co- and K-doped iron pnictides. Europhys. Lett. 87, 37001 (2009).
23. Christianson, A. D. et al. Static and Dynamic Magnetism in Underdoped Superconductor BaFe$_{1.95}$Co$_{0.05}$As$_2$. Phys. Rev. Lett. 103, 087002 (2009).
24. Pratt, D. K. et al. Dispersion of the superconducting spin resonance in underdoped and antiferromagnetic BaFe$_2$As$_2$. Phys. Rev. B 81, 140510(R) (2010).
25. Tucker, G. S. et al. Magnetic excitations in underdoped Ba(Fe$_{1-x}$Co)$_2$As$_2$ with x = 0.047. Phys. Rev. B 86, 024505 (2012).
26. Zhang, Q. et al. Neutron-Scattering Measurements of Spin Excitations in LaFeAsO and Ba(Fe$_{0.955}$Co$_{0.047}$)$_2$As$_2$: Evidence for a Sharp Enhancement of Spin Fluctuations by Nematic Order. Phys. Rev. Lett. 114, 057001 (2015).
27. Wang, M. et al. Experimental elucidation of the origin of the ‘double spin resonances’ in Ba(Fe$_{1−x}$Co)$_2$As$_2$. Phys. Rev. B 93, 205149 (2016).
28. Wang, C. et al. Longitudinal Spin Excitations and Magnetic Anisotropy in Antiferromagnetically Ordered BaFe$_2$As$_2$. Phys. Rev. X 3, 041036 (2013).
29. Fidyusiak, M. Origin of longitudinal spin excitations in iron-pnictide parent compounds. Eur. Phys. J. B 89, 41 (2016).
30. Harriger, L. W. et al. Nematic spin fluid in the tetragonal phase of BaFe$_2$As$_2$. Phys. Rev. B 84, 045444 (2011).
31. Zhang, W. et al. Effect of Nematic Order on the Low-Energy Spin Fluctuations in Detwinned BaFe$_{1.935}$Ni$_{0.065}$As$_2$. Phys. Rev. Lett. 117, 227003 (2016).
32. Hu, W. Z. et al. Origin of the Spin Density Wave Instability in AFe$_2$As$_2$ (A = Ba, Sr) as Revealed by Optical Spectroscopy. Phys. Rev. Lett. 101, 257005 (2008).
33. Nakajima, M. et al. Evolution of the optical spectrum with doping in Ba(Fe$_{1−x}$Co)$_2$As$_2$. Phys. Rev. B 81, 104528 (2010).
34. Braden, M. et al. Anisotropy of the Incommensurate Fluctuations in Sr$_2$RuO$_4$: A Study with Polarized Neutrons. Phys. Rev. Lett. 92, 097402 (2004).
35. Mishra, V., Scalapino, D. J. & Maier, T. A. s$^4$ pairing near a Lifshitz transition. Sci. Rep. 6, 32078 (2016).
36. Souma, S. et al. The origin of multiple superconducting gaps in MgB$_2$. nature 423, 65 (2003).
37. Brown, P. J. Spherical Neutron Polarimetry, in Neutron Scattering from Magnetic Materials, Edt. T. Chatterji, Elsevier B.V. (2006).

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Author Contributions
K.K. and C.H.L. grew the crystal; F.W., C.H.L., K.K., P.S., K.S., N.Q. and M.B. participated in the experiments; F.W., C.H.L. and M.B. analyzed the data; F.W. and M.B. wrote the paper with input from all authors.

Additional Information
Competing Interests: The authors declare that they have no competing interests.

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