Extrapolation Techniques and Systematic Uncertainties in the NOνA Muon Neutrino Disappearance Analysis

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The NOνA long-baseline neutrino experiment consists of two highly active, finely segmented, liquid scintillator detectors located 14 mrad off Fermilab’s NuMI beam axis, with a Near Detector located at Fermilab, and a Far Detector located 810 km from the target at Ash River, MI. NOνA released its first preliminary results of the muon neutrino disappearance parameters, measuring \( \sin^2(\theta_{23}) = 0.51 \pm 0.10 \) and or the normal hierarchy \( \Delta m^2_{32} = 2.37^{+0.16}_{-0.15} \times 10^{-3} \text{ eV}^2 \) and for the inverted hierarchy \( \Delta m^2_{32} = -2.40^{+0.14}_{-0.17} \times 10^{-3} \text{ eV}^2 \). This talk will present a discussion of the systematic uncertainties and extrapolation methods used for this first analysis which uses \( 2.74 \times 10^{20} \) POT-equivalent collected between July 2013 and March 2015.

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1 Introduction

The NO\(\nu\)A experiment, a long baseline neutrino oscillation experiment, consists of two almost completely active, segmented, liquid scintillator detectors. The 0.3 kton Near Detector (ND) is located on site at Fermilab, 105 m underground and 1 km away from Fermilab’s NuMI beam production target. The 14 kton Far Detector (FD) is located at Ash River, Minnesota, 810 km away from Fermilab’s NuMI neutrino source. The FD building is covered by a 3 m equivalent mound of barite rock. This provides an overburden of more than ten radiation lengths to reduce background from cosmic rays. The relative sizes of the detectors are shown diagrammatically in Figure 1.

![Figure 1: The relative sizes of the NO\(\nu\)A Far and Near Detectors. The structure of the NO\(\nu\)A detector layers is also shown.](image1.png)

The two detectors are located 14.6 mrad off the NuMI beam axis, resulting in a relatively narrow neutrino energy band centered at 2 GeV, where the \(\nu_\mu(\bar{\nu}_\mu) \rightarrow \nu_e(\bar{\nu}_e)\) oscillation maximum occurs (see Figure 3). This narrow band beam results not only in a increased flux of events at 2 GeV events but also in a suppression of the neutral current background which is very important for \(\nu_\mu\) to \(\nu_e\) measurements. The neutrino energy relies on the angle between pion decay and neutrino interaction inside the detector. As one goes to an off-axis location the dependence on pion energy becomes flat.

Both NO\(\nu\)A detectors are highly segmented tracking calorimeters built in their entirety from low Z (0.18 radiation lengths per layer) and highly reflective (15% TiO\(_2\)) PVC cells [1]. The PVC cells are filled with liquid scintillator consisting of mineral oil infused with 5% pseudocumene. The detectors are constructed from extrusions consisting of planes of 6 cm \times 4 cm cells, where each cell extends the full width or height of the detector. These PVC extrusions are assembled in alternating layers either vertically or horizontally, as can be seen in Figure 1. This orientation of the cells allows for 3D event reconstruction. In total there are 344,054 cells in the FD.
and 21,192 cells in the ND. The scintillation light is collected in every cell by a loop of wavelength shifting fiber and each cell is read out individually, using 32-pixel avalanche photo-diodes (APDs).

The NOνA FD has been taking data since July 2013, taking advantage of the modular nature of NOνA. The first data was recorded with the first 1 kton block of the detector, with additional kton blocks being added once they were fully commissioned. This allowed for the detector to take data as it was constructed. Both NOνA detectors have been fully constructed and commissioned since August 2014. As the detector volume was changing size as the early data was recorded this information is encoded in POT quoted, hence exposure is giving the POT-14-ton-equivalent.

The first results from the NOνA experiment were presented in August 2015 and these proceedings will present a discussion of the systematic uncertainties associated with the analysis of first $2.74 \times 10^{20}$ POT-equivalent collected for the muon-neutrino disappearance analysis. This data was collected between July 2013 and March 2015. The methods developed to predict the FD spectrum as extrapolated from the observed ND data will also be presented.

2 Near to Far Detector Extrapolation Method

The neutrino energy spectrum at the NOνA ND is measured close to the neutrino source before neutrino oscillations have occurred. This large statistics data sample is used to validate the Monte Carlo (MC) prediction of the expected beam flux and the simulation of the detector response. All beam intrinsic backgrounds can be measured at the ND to a high precision.

NOνA uses the ND energy spectrum to make a prediction of the energy spectrum that will be seen at the NOνA FD. This prediction technique is known as extrapolation and reduces the dependence on systematics uncertainties which apply to both detectors. NOνA employs a direct extrapolation technique where the ratio of the FD to ND flux, as determined from MC, was used to predict the expected FD energy spectrum from the measured ND energy spectrum. This extrapolation is performed bin-by-bin in reconstructed energy. To extend the extrapolation technique beyond the prediction of the null oscillation spectrum, migration matrixes are used to apply corrections to the measured ND reconstructed energy spectra to obtain the MC true energy spectra. This allows for oscillation probability predictions to be applied. To fully qualify the oscillation parameters that describe the observed FD spectrum we minimize $\chi^2$ between observed FD data best-fit, fitted using the full systematic suite (described in Section 3), and the predicted FD spectrum under different oscillation predictions. The full three-flavor parameterization of neutrino oscillations is used, with the other oscillation parameters and their uncertainties marginalized over. The oscillation parameters included in fit are; $\Delta m^2_{21} = 7.53 \pm 0.18 \times 10^{5}\text{eV}^2$;
\[ \sin^2(2\theta_{13}) = 0.086 \pm 0.005; \sin^2(2\theta_{12}) = 0.846 \pm 0.021; \text{ and } \delta_{CP} \text{ is unconstrained.} \]

As the two detectors are functionally identical this ratio based method allows for reductions in detector-response, object-identification, and energy reconstruction based uncertainties. Slight differences in acceptance, due to the size of the detector, and in the flux lead to not complete cancellation of systematics uncertainties. The MC flux prediction results in one of the largest single detector systematic uncertainties. The two detectors see slightly different fluxes so this uncertainty does not cancel completely. This arises as the ND sees a line source around 14.6 mrad where as the FD a point source at exactly 14.6 mrad, see Figure 3.

The NO\(\nu\)A experiment performs a blinded analysis technique where are all tools and algorithms are constructed using simulations or side band regions, only once an analysis is classified, by the collaboration, to be complete is the analysis run over the FD data.

![Figure 3: The energy spectrum for \(\nu_\mu\) charged current events both on-axis (open histogram) and 14.6 mrad off-axis (red histogram), in the NuMI beam. The left spectrum is for the NO\(\nu\)A FD and the right is for the ND.](image)

### 3 Systematic Uncertainties

I will discuss the non-negligible systematic uncertainties associated with the NO\(\nu\)A muon neutrino disappearance analysis. Multiple other effects were considered, for example the detector response modeling and the attenuation calibration corrections, but will not be discussed here as they were determined to be negligible. A summary of all the non-negligible systematic uncertainties is given in Table 1.

a) **Uncertainty of Background Rates**

The only non-negligible contaminations in the in the selected muon-neutrino sample
(backgrounds) for the muon-neutrino disappearance analysis are the neutral current and tau neutrino backgrounds. These contamination rates are estimated from simulation and a 100% uncertainty is taken on them.

The largest background at the NOνA FD is the rate of cosmic muons. This rate is determined from minimum-bias data taking outside of the neutrino beam spill. The statistical uncertainty of this minimum-bias sample is negligible, as along with each beam spill a much larger (35x) minimum-bias sample is recorded. This sample is recorded using the same detector conditions so they can be directly matched.

b) Calibration uncertainty: Absolute Hadronic Energy Scale
The NOνA experiment uses muons which stop in the detector to provide a standard candle for setting the absolute energy scale. The uncertainty on this is estimated from maximum difference between the multiple probes of calibration which are available at NOνA. The observed difference is propagated through the full analysis framework, including the extrapolation and oscillation parameter minimization. The probes available at NOνA include the Michele electrum spectrum, the π⁰ mass peak and the \(dE/dx\) of the muon and the proton. Using this method a 5% percent absolute and a 5% relative calibration uncertainty are determined.

Comparing the the off-track energy measured in NOνA ND charged current muon-neutrino interactions to the simulation a discrepancy is seen. We define off-track energy to be the sum of all energy associated with the neutrino interaction that is not part of the muon track. This is referred to as Hadronic Energy. As the NOνA detectors are located off-axis the location of the neutrino energy peak at this location is known to a high precision. Therefore we use this knowledge to tune the hadronic energy such at the neutrino energy is peaked, as expected, at 2 GeV. Using the ND data a 21% hadronic energy correction is determined. This correction translates into a 6% correction to the neutrino energy. We conservatively take a 100% absolute uncertainty on this correction. This is our largest systematic uncertainty. Combining this correction with the absolute hadronic energy scale we get a 22% total absolute hadronic energy uncertainty.

c) Calibration uncertainty: Relative Hadronic Energy Scale
In addition, we calculate the relative hadronic energy uncertainty due to the different detector acceptances. As the 21% correction factor is calculated using ND data it may be optimized only for the ND. Due to the smaller size of the ND the acceptance is sculpted as compared to the FD and a higher percentage of the events that pass the selection are quasi-elastic. This effect is investigated by allowing the normalization and the energy scale of deep inelastic scattering, resonant and quasi-elastic events (as defined by GENIE [2]) to float. A three parameter simultaneous fit of the muon energy, the off-track energy and normalization is done. The difference be-
Figure 4: The distribution of the off-track energy (left) and the reconstructed neutrino energy (right) shown for both the simulated ND events (red) and the recalibrated ND data (blue) after the 21% correction factor is applied.

tween the one-parameter 21% scaling and this interaction-dependent scaling is used to determine the relative uncertainty. A 2% relative uncertainty and 1% relative normalization uncertainty are determined. The relative uncertainty is combined with the uncertainty discussed in b) to give a 5% total relative hadronic energy uncertainty. The distribution of the off-track energy and the reconstructed neutrino energy at the NO\(\nu\)A ND are shown in Figure 4.

d) Flux Uncertainties
The NO\(\nu\)A flux is modeled using FLUKA/FLUGG [3]. For each individual detector the flux uncertainty is large (20% at the 2 GeV peak) and dominated by the hadron production uncertainties. The hadron production uncertainties are estimated by comparing the NuMI target MC predictions to the the thin-target data from NA49 [4]. The hadron transport uncertainties were also investigated. Uncertainties due to the NuMI target and horn positions, the horn current and the magnetic field, and the beam spot size and position were determined to be small compared to hadron production uncertainties and are considered negligible. The flux uncertainties are highly correlated between the two detectors. For each individual detector the flux uncertainty is large but due to the use of the extrapolation method it is the ratio of the uncertainties that is relevant. As the fluxes are very highly correlated between the two detectors the flux uncertainty is reduced to the percent level. The fraction uncertainty on the NO\(\nu\)A ND and FD and the ratio is shown in Figure 5.

e) Absolute Normalization
There are two sources of absolute normalization uncertainty on NO\(\nu\)A. The first arises from the an uncertainty in the detector mass which leads to uncertainty in the exposure. The NO\(\nu\)A detectors are constructed from PVC cells which are filled with a liquid scintillator. Each cell contains a loop of wavelength shifting fiber. These
Figure 5: The NOνA flux uncertainty for the far detector (left), near detector (middle) and the ratio (right).

cells are extruded in sets of 16 which are glued together to make a plane of the detector. A 0.7% normalization uncertainty is taken on the amount of plastic, glue, scintillator and wavelength shifting fiber. This is determined from the uncertainties on these components as built and as compared to what is in the simulation. The second source of absolute normalization is due to a potential proton-on-target, POT, skew between the two detectors. As data taking at the ND and FD was over different periods if there had been a POT mis-measurement this could result in a normalization skew. The NuMI beam has been shown to be very stable and a conservative 0.5% proton-on-target normalization uncertainty is taken. Combining this with the mass uncertainty gives an overall 0.9% normalization uncertainty.

f) Neutrino Interaction Modeling
NOνA uses GENIE to study the uncertainty on cross sections and final state particles exiting the nucleus. The effect of 1 and 2 $\sigma$ variations of the 67 parameters provided in GENIE on the muon-neutrino charged-current energy spectrum was studied. Of these 67 parameters only 6 were seen to have a noticeable effect. There are; the axial mass of the charged current quasi-elastic cross section; the axial mass of the neutral current quasi-elastic cross section; the axial mass of the charged current resonant cross section; the axial mass of the neutral current resonant cross section; the vector mass for the charged current resonant cross section; and the vector mass for the neutral current resonant cross section. As well as these 6 largest, and an effective parameter that includes the effect of the other 61 parameters added in quadrature, was added as penalty terms in the fit. From this a 10 - 25% uncertainty on neutrino interaction dynamics was determined but again this uncertainty mostly cancels out due to the use of a ratio method.
Table 1: Summary table of the non-negligible systematics in NO\(\nu\)A muon neutrino oscillation measurement.

| Systematic                                      | Value (1\(\sigma\)) | Best fit (\(\sigma\)) |
|-------------------------------------------------|----------------------|------------------------|
| Bkg. (neutral current and \(\nu_\tau\))         | 100%                 | 0.06                   |
| Absolute Normalization                          | 1.3%                 | 0.0008                 |
| Absolute Hadronic energy scale                  | 22%                  | -0.67                  |
| Absolute energy scale                           | 1%                   | 0.06                   |
| Beam                                            | Energy dependent     | -0.02 (20% at 2 GeV)   |
| Relative Normalization                          | 1.4%                 | -0.03                  |
| Relative Hadronic energy scale                  | 5.4%                 | 0.05                   |
| GENIE \(M_a\)                                   | 15-25%               | -0.18                  |
| GENIE \(M_\nu\)                                 | 10%                  | -0.06                  |

4 Results

NO\(\nu\)A predicted a event rate of 201 \(\nu_\mu\) charge current events at its FD extrapolated from the ND data, in range 0 – 5 GeV. This included a predicted background of 1.4 \(\pm\) 0.2 comic muons determined from minimum-bias data and 2.0 \(\pm\) 2.0 neutral current and \(\nu_\tau\) events determined from simulation. An observed FD \(\nu_\mu\) charge current rate of 33 events was seen, giving a clear signature of neutrino oscillations. Using these results the atmospheric neutrino oscillation parameters were measured to be \(\sin^2(\theta_{23}) = 0.51 \pm 0.10\) and \(\Delta m^2_{32} = 2.37^{+0.16}_{-0.15} \times 10^{-3}\) eV\(^2\) for the normal hierarchy and \(\Delta m^2_{32} = -2.40^{+0.14}_{-0.17} \times 10^{-3}\) eV\(^2\) for the inverted hierarchy. The energy spectrum of the observed events, along with the best-fit distribution to these events (with and without systematics) is shown in Figure 6. The best-fit point along with the 68% and 90% contours in \(\sin^2(\theta_{23}) - \Delta m^2_{32}\) space for the normal hierarchy is also shown.

5 Conclusion

In conclusion, the extrapolation methods and systematic uncertainties associated with the analysis of the first data for the muon-neutrino disappearance analysis at NO\(\nu\)A have been described. This corresponded to \(2.74 \times 10^{20}\) POT-equivalent collected between July 2013 and March 2015. This analysis is statistically limited and all systematic uncertainties are dominated by the absolute hadronic energy scale uncertainty. Fully quantifying the hadronic response will be essential for the next generation of results. With these results NO\(\nu\)A has showcased its ability to produce world class physics and to be a leader in precision atmospheric neutrino oscillations measurements. With only 7.6% of the nominal final statistics NO\(\nu\)A is already competitive
Figure 6: The energy spectrum of the observed events, along with the best fit distribution to these events (with and without systematics) (right). The best fit point along with the 68% and 90% contours in $\sin^2(\theta_{23}) - \Delta m^2_{32}$ space for the normal hierarchy (left).

with the world limits.

References

[1] D. S. Ayres et al. [NOvA Collaboration], (2005) [hep-ex/0503053](http://arxiv.org/abs/hep-ex/0503053).
[2] C. Andreopoulos et al (2010), Nucl. Instrum. Meth. A614, 87-104.
[3] A. Ferrari, P. R. Sala, A. Fasso, and J. Ranft, (2005), CERN-2005-010.
[4] C. Alt et al. [NA49 Collaboration], Eur. Phys. J. C 49 897 (2007), T. Anticic et al. [NA49 Collaboration], Eur. Phys. J. C 68 1 (2010).