Clumping in the Winds of Wolf–Rayet Stars

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Abstract

We attempt to determine the driver for clumping in hot-star winds by extending the measure of the spectral variability level of Galactic Wolf–Rayet stars to by far the hottest known among them, the WN2 star WR 2 and the WO2 stars WR 102 and WR 142. These three stars have \(T_\ast = 140\) and 200 kK, the last two being well above the bulk of WR stars with \(T_\ast \approx 40–120\) kK. This full temperature range for WR stars is much broader than that of their O-star progenitors (\(~30–50\) kK), so is better suited to look for any temperature dependence of wind clumping. We have obtained multiple observations with high signal-to-noise, moderate-resolution spectroscopy in search of small-scale variability in the strong emission lines from the dense winds of these three extreme stars, and find a very low-level of variability in both stars. Temperature and terminal velocity are correlated, so faster winds show a lower variability, though this trend goes against any predictions made involving Line Deshadowing Instability (LDI) only, implying that instabilities intrinsic to LDI are not the main source of wind clumping. Instead, it could be taken as support for the suggestion that clumps are caused by a subsurface convection zone (SSCZ) at \(T \sim 170\) kK, since such an SSCZ would have little opportunity to operate under the hydrostatic surface of these hottest WR stars. It is still possible, however, that an SSCZ-related driver could interact with nonlinear line instability effects to enhance or possibly even produce clumps.

Unified Astronomy Thesaurus concepts: Wolf-Rayet stars (1806); Stellar winds (1636); Stellar convective zones (301); Radiative transfer (1335)

1. Introduction

The discovery more than 30 yr ago of stochastic clumps in the winds of two Wolf–Rayet (WR) stars (Schumann & Seggewiss 1975; Moffat et al. 1988) led to the current evidence that most, if not all, hot-star winds are pervaded by hierarchies of thousands of small, randomly varying clumps (Eversberg et al. 1998; Lépine & Moffat 1999, 2008; Grosdidier et al. 2001). This fundamental discovery has had a profound effect on our understanding of hot stellar winds, perhaps the most important of which is the necessary reduction in the estimated mass-loss rates by a factor of 2–5 (Moffat & Robert 1994). This in turn affects the whole evolutionary history of massive stars, where mass-loss plays a crucial role (Maeder & Meynet 2000; Ekström et al. 2012).

But the question of the origin of these structures remains uncertain and controversial. On the one hand, clumps can be generated spontaneously in the wind by the inherently unstable nature of radiative line driving (Lucy & White 1980; Owocki et al. 1988), known as line deshadowing instability (LDI, equivalently Line Driven Instability; Owocki & Rybicki 1984; Sundqvist & Owocki 2013). Based on this theory, all hot stars should have clumpy winds, especially the hotter ones, since multiplying the flow time by the growth rate of small-scale line-driven perturbations yields of order \(\nu/\nu_{th} \sim 100\) in all but the most extreme cases of multiple scattering (Gayley & Owocki 1995).

On the other hand, it has been claimed that stochastic wind variability of WR stars may be higher in cooler stars (Michaux et al. 2014), which would require an explanation separate from the predictions of the LDI theory. Classical WR stars, the late He-burning stage of stars with an initial mass above \(\sim 25\ M_\odot\), as well as WNs, which are H-rich very massive main-sequence stars, have the strongest stable winds of all hot luminous stars, making them ideal candidates to study optical wind variations. The work by Michaux et al. (2014) compiles the measurements of the line profile variability (lpv) amplitude, \(\sigma\), of 64 Galactic WR stars. This sample includes WR stars of all subtypes in both the WN and WC sequences, and covers surface temperatures (which correlate well with the wind temperatures) between 40 and 140 kK.

If confirmed, this trend could suggest that another mechanism at the origin of the clumps may be at play, possibly even surpassing the role of the inherent LDI instability. One candidate mechanism is the subsurface convection (SSC) regions associated with a partial ionization zone (PIZ) of iron at \(T \sim 170\) kK in luminous hot stars (Cantiello et al. 2009). Grassitelli et al. (2016) has already claimed that a subsurface convective region is found in all their models of H-free WR stars in the range of \(2–17\ M_\odot\). When the stochastic motions associated with this convection reach the (radiative) stellar surface, they could generate clumpy structures, altering the driving of mass flux through the critical point, thereby altering the density or the radiative flux at the surface. If that mechanism is the main driver of clumps, it implies that slower and cooler winds are clumpier, since such stars have cooler surfaces and deeper and denser subsurface convection zones. Since smaller, hotter stars have higher escape speeds and faster winds, temperature provides an effective lever for distinguishing these possible sources for clumping.

In this study, we revisit the trend presented by Michaux et al. (2014) by adding 29 stars and recalculating the \(\sigma\) values uniformly for the whole sample. Two of the new stars are WR 102 and WR 142, both of subtype WO2; they are by far the hottest among known Galactic WR stars with \(T_\ast = 200\) kK (Sander et al. 2012). We also revisit the star WR 2 (WN2b), the hottest known Galactic WN star (\(T_\ast = 141.3\) kK, Hamann et al. 2006), for which no clump-related lpv has been found at, or above a level of 1% of the line intensity (Chené & St-Louis 2008), in
contrast with all other observed WR stars (Robert 1992; Lépine & Moffat 1999; Chené & St-Louis 2011). These three hot WR stars at the extreme limit offer an opportunity to test if the amplitude of lpv depends significantly on the wind temperature and, consequently, if the origin of the hot stellar wind clumps involves a mechanism like subsurface convection. In Section 2, we present our new observations and describe how we carried out the data reduction. Section 3 relates how we carried out the uniform evaluation of the level of spectroscopic variability and Section 4 discusses the special case of the three hottest stars in our sample. We discuss our results in Sections 5 and 6 and conclude in Section 7.

2. Observations and Reduction

The data used for most of the stars in this study have already been published in St-Louis et al. (2009), Chené & St-Louis (2011), and Grassitelli et al. (2016) (see Section 3). However, new spectra were observed for WR 2, WR 102, and WR 142 using the GMOS spectrographs at Gemini-North and Gemini-South (see Table 1 for details on the observing campaigns).

For these observations, we reached a 1.5 Å spectral resolution ($R \sim 3400$), which is ideal for resolving the typical small-scale variations due to clumps seen in all other well-observed WR stars. The rapid cadence of observation ($\sim 140$ s between each spectrum) allows us to prevent motion blur of the variations due to rapidly accelerating clumps.

The bias subtraction, flat-fielding, spectrum extraction, sky subtraction, and wavelength calibration of all spectra were executed in the usual way using the Gemini IRAF$^4$ package.

Special care was taken for the normalization of the spectra. First, a mean was made for each of the series that were taken during the same night. Then each spectrum of a given night was divided by the night mean and the ratio fitted with a low-order Legendre polynomial (between fourth and eighth order). The original individual spectra were divided by this fit and were therefore at the same level as the night mean. Once this procedure was completed for each night, the night means were then put at the same level by using the same procedure as described above, and a global, high quality mean was produced. This final mean spectrum was used to put all individual spectra of the entire run at the same level and was also fitted in selected pseudo-continuum regions, defined as wavelength regions where large emission lines do not dominate. These regions lie on the straight horizontal lines in Figure 1. This fit was applied to all individual spectra, so they become normalized by the continuum in a uniform way. The error on the continuum normalization measured as the standard deviation of individual spectra around the continuum function is typically 0.5% per pixel.

3. Recalculating the $\sigma$ Values

3.1. Determining $\sigma$

Since a few cases presented by Michaux et al. (2014) were moderate outliers, and because we are merging values published in separate studies, we recalculated the $\sigma$ values for all the observed WR stars in a uniform way, with a much better control of the systematics.

We worked from the reduced and normalized spectra published in St-Louis et al. (2009), Chené & St-Louis (2011), and Grassitelli et al. (2016), and observed with the 1.6 m telescope at the Observatoire du Mont Mégantic, the 1.5 m telescope at the Cerro-Tololo International Observatory, and the Gemini Observatory.$^5$

These sources have a total of four to five observed spectra per star, which allows one to determine the statistical significance of the observed changes using the Temporal Variance Spectrum (TVS) formalism as introduced by Fullerton et al. (1996). The square root of the TVS, which divided by the detection threshold becomes $\Sigma$, is proportional to the amplitude of variability at each wavelength, and is compared with a detection threshold. For stars with a significant detection of lpv, we calculate the $\sigma$ value, extracted from the $\sigma$ spectrum, as introduced by St-Louis et al. (2009). The $\sigma$ spectrum differs from the $\Sigma$ spectrum, in the sense that instead of comparing the variance at a given pixel with the noise in the neighboring continuum, it compares the variance of a given pixel with the noise in that same pixel. The advantage over $\Sigma$ is that it gives the amplitude of the variability relative to the intensity of the line over which it was observed. In other words, it gives a measure of how high in percentage of the line intensity the amplitude of the lpv is.

The equation for $\Sigma$ diverges when it gets too close to the continuum, as it has no meaning outside of emission lines. That is why we can only determine $\sigma$ around the center of the lines, avoiding the low intensity part of the wings. It is for that reason, and for another reason that will be discussed shortly...

Table 1: Observing Campaigns Description

| Star Name | Wavelength Coverage | Exposure Time per frame | S/N (Continuum) per frame | Number of Spectra | Program ID |
|-----------|---------------------|-------------------------|---------------------------|-------------------|------------|
| WR 2      | 3970-5435 Å         | 120 s/250 s             | ~125                      | 68                | GN-2012B-Q-115 |
| WR 102    | 4380-6000 Å         | 120 s                   | ~50                       | 82                | GS-2017B-Q-62  |
| WR 142    | 4370-6100 Å         | 120 s                   | ~100                      | 74                | GN-2017B-Q-6   |

Figure 1. Average of all the Gemini spectra observed during our campaigns for the three stars WR 2 (WN2b), WR 102 (WO2), and WR 142 (WO2). The spectra are arbitrarily shifted vertically from one star to the next for clarity. The dashed horizontal line for each star marks the rectified continuum level.

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$^5$ Program IDs: GS-2008B-Q-87, GS-2010B-Q-58, GN-2010B-Q-78, GN-2010B-Q-119, GS-2014A-Q-42, GS-2014A-Q-73, and GN-2018B-Q-404.
| WR | Group | Spectral Type | $T_{\text{eff}}$ (K) | $\sigma$ (%) | sp. Line C III/IV $\lambda$ | Line int. ($F_{\text{cont}}$) | Line FWHM (km s$^{-1}$) | Note |
|----|-------|---------------|-----------------------|-------------|---------------------|----------------------|-----------------------|------|
| 103 | (a)   | WC9d          | 45                    | 3.34 ± 1.52 | 5696                | 10.6                 | 1018                  |      |
| 106 | (a)   | WC9d          | 45                    | 2.49 ± 1.13 | 5696                | 12.4                 | 966                   |      |
|     |       |               |                      | 3.76 ± 1.58 | 5808                | 3.4                  | 1463                  |      |
| 119 | (a)   | WC9d          | 45                    | 3.17 ± 1.27 | 4659                | 7.6                  | 932                   |      |
|     |       |               |                      | 2.80 ± 1.63 | 5696                | 11.8                 | 936                   |      |
|     |       |               |                      | 3.26 ± 1.72 | 5808                | 3.1                  | 1405                  |      |
| 121 | (a)   | WC9d          | 45                    | 4.97 ± 3.27 | 4659                | 7.5                  | 968                   |      |
|     |       |               |                      | 4.80 ± 1.42 | 5696                | 11.2                 | 936                   |      |
|     |       |               |                      | 5.47 ± 1.98 | 5808                | 2.9                  | 1434                  |      |
| 81  | (a)   | WC9           | 45                    | 3.44 ± 1.68 | 5696                | 11.7                 | 1099                  |      |
|     |       |               |                      | 5.57 ± 1.84 | 5808                | 3.4                  | 1396                  |      |
| 92  | (a)   | WC9           | 45                    | 5.37 ± 2.39 | 5696                | 9.3                  | 977                   |      |
|     |       |               |                      | 5.91 ± 1.55 | 5808                | 2.6                  | 1436                  |      |
|     |       |               |                      | 5.52 ± 3.33 | 5880                | 2.9                  | 3392                  |      |
| 53  |       | WC8d          | 50                    | 3.60 ± 1.31 | 5696                | 11.5                 | 1752                  |      |
|     |       |               |                      | <2.92       | 5808                | 5.5                  | 1358                  |      |
|     |       |               |                      | <2.92       | 5880                | 2.8                  | 2092                  |      |
| 57  | (b)   | WC8           | 63                    | 3.47 ± 0.96 | 5696                | 5.9                  | 2363                  |      |
|     |       |               |                      | <2.49       | 5808                | 6.7                  | 1637                  |      |
| 77  | (b)   | WC8           | 63                    | 2.16 ± 0.55 | 5696                | 4.9                  | 2117                  | b    |
|     |       |               |                      | 2.79 ± 0.58 | 5808                | 4.3                  | 1875                  |      |
| 135 | (b)   | WC8           | 63                    | 1.94 ± 0.61 | 5696                | 6.5                  | 1988                  |      |
|     |       |               |                      | 0.96 ± 0.22 | 5808                | 8.0                  | 1434                  |      |
| 14  | (c)   | WC7           | 71                    | 2.57 ± 0.47 | 5696                | 2.9                  | 2852                  |      |
|     |       |               |                      | 1.28 ± 0.29 | 5808                | 9.3                  | 1917                  |      |
| 50  | (c)   | WC7           | 71                    | 2.03 ± 0.43 | 5696                | 2.5                  | 3745                  |      |
|     |       |               |                      | 1.14 ± 0.34 | 5808                | 5.9                  | 2394                  |      |
| 90  | (c)   | WC7           | 71                    | 1.61 ± 0.25 | 5696                | 3.1                  | 3094                  | b    |
|     |       |               |                      | 0.68 ± 0.10 | 5808                | 8.1                  | 2194                  |      |
| 132 | (c)   | WC6           | 71                    | 1.48 ± 0.60 | 5696                | 3.4                  | 3214                  |      |
| 5   | (d)   | WC6           | 79                    | 1.33 ± 1.38 | 4659                | 24.3                 | 2459                  | c    |
| 13  | (d)   | WC6           | 79                    | 1.84 ± 0.58 | 5696                | 2.2                  | 3047                  | b    |
| 27  | (d)   | WC6           | 79                    | 1.35 ± 1.02 | 5696                | 2.9                  | 3048                  |      |
|     |       |               |                      | 1.68 ± 0.80 | 5808                | 17.6                 | 2086                  |      |
| 45  | (d)   | WC6           | 79                    | 1.03 ± 0.61 | 4659                | 20.1                 | 2432                  |      |
| 154 | (d)   | WC6           | 79                    | 0.64 ± 1.33 | 4659                | 19.9                 | 3019                  | e    |
| 4   | (d)   | WC5           | 79                    | 1.67 ± 1.46 | 4659                | 23.5                 | 3179                  |      |
| 32  | (d)   | WC5           | 79                    | 0.97 ± 0.34 | 4659                | 20.7                 | 2966                  |      |
| 41  | (d)   | WC5           | 79                    | 0.76 ± 0.32 | 4659                | 17.7                 | 4279                  |      |
|     |       |               |                      | 1.18 ± 1.09 | 5696                | 2.4                  | 4657                  |      |
|     |       |               |                      | 0.88 ± 0.32 | 5808                | 21.1                 | 3090                  |      |
| 15  | (e)   | WC6           | 79                    | <2.58       | 5696                | 2.3                  | 4722                  | b    |
| 23  | (e)   | WC6           | 79                    | <2.06       | 5696                | 2.4                  | 3627                  | b    |
| 17  | (e)   | WC5           | 79                    | <1.78       | 5696                | 1.3                  | 2689                  |      |
| 33  | (e)   | WC5           | 79                    | <1.35       | 5696                | 11.4                 | 3750                  |      |
| 111 | (f)   | WC5           | 89                    | 0.70 ± 0.16 | 5808                | 20.2                 | 2324                  |      |
| 150 | (f)   | WC5           | 89                    | 0.93 ± 0.54 | 5808                | 21.4                 | 3307                  |      |
| 52  |       | WC4           | 112                   | <3.68       | 5808                | 16.3                 | 2436                  | d    |
| 144 |       | WC4           | 112                   | 1.18 ± 1.26 | 6750                | 3.5                  | 4294                  | c    |
| 143 |       | WC4           | 120                   | 1.38 ± 1.49 | 4659                | 7.9                  | 4602                  | c    |
| 102 |       | WO2           | 200                   | <0.25       | 5808                | 2.4                  | 3539                  |      |
| 142 |       | WO2           | 200                   | 0.12 ± 0.10 | 5808                | 1.9                  | 3295                  |      |

Notes.

a From Sander et al. (2012).

b Affected by variable continuum.

c Affected by continuum normalization issue.

d Variations close to the detection threshold.

e Our results are presented in Table 2 for WC and WO stars, in Table 3 for WN stars, in Table 4 for WNH stars, and in Table 5 for WN/WC stars.
Table 3: WN Stars without H

| WR  | Group         | Spectral Type | Teff\(^{a}\) (kK) | \(\sigma\) (%) | sp. Line He II \(\lambda\) | Line int. \((F_{\text{cont}})\) | Line FWHM \((\text{km s}^{-1})\) | Note |
|-----|---------------|---------------|-------------------|----------------|------------------------|------------------|-------------------|------|
| 123 | WNe8(WNE-w)   | WNe8(WNE-w)   | 44.7              | 5.13 ± 3.29     | 4686                   | 3.6              | 725               |      |
| 84  | (a) WNe7(WNE-w) | WNe7(WNE-w)   | 50.1              | 5.58 ± 1.73     | 4686                   | 1.8              | 844               |      |
| 120 | (a) WNe7(WNE-w) | WNe7(WNE-w)   | 50.1              | 6.24 ± 2.45     | 5411                   | 2.4              | 815               |      |
|     |               | WNe7(WNE-w)   |                   | 6.27 ± 1.15     | 4860                   | 2.0              | 776               |      |
| 115 | (a) WNe6-w    | WNe6-w        | 50.1              | 7.70 ± 1.58     | 4686                   | 5.1              | 1149              |      |
|     |               | WNe6-w        |                   | 8.31 ± 1.89     | 5411                   | 1.9              | 967               |      |
| 55  | (b) WNe7(WNE-w) | WNe7(WNE-w)   | 56.2              | 8.16 ± 1.98     | 5411                   | 2.3              | 858               |      |
| 67  | (b) WNe6-w    | WNe6-w        | 56.2              | 4.99 ± 1.83     | 5411                   | 2.3              | 1028              |      |
| 71  | (b) WNe6-w    | WNe6-w        | 56.2              | 4.17 ± 1.19     | 5411                   | 2.3              | 1114              |      |
| 75  | (c) WNe6-s    | WNe6-s        | 63.1              | 4.25 ± 1.35     | 5411                   | 2.2              | 2785              |      |
| 134 | WNe6-s       | WNe6-s        | 63.1              | 8.86 ± 1.68     | 4686                   | 10.6             | 2639              |      |
| 83  | (c) WNe5o     | WNe5o         | 63.1              | 2.81 ± 0.97     | 5411                   | 2.1              | 1071              |      |
| 42d | (c) WNe5b     | WNe5b         | 63.1              | 3.94 ± 1.22     | 4686                   | 3.3              | 3390              |      |
| 20  | (c) WNe5-w    | WNe5-w        | 63.1              | 4.02 ± 0.99     | 4686                   | 7.4              | 1575              |      |
|     |               | WNe5-w        |                   | 4.52 ± 1.18     | 5411                   | 2.5              | 1233              |      |
| 34  | (c) WNe5-w    | WNe5-w        | 63.1              | 5.62 ± 1.39     | 4686                   | 9.0              | 1529              |      |
|     |               | WNe5-w        |                   | 4.99 ± 2.23     | 5411                   | 2.6              | 1324              |      |
| 54  | (c) WNe5-w    | WNe5-w        | 63.1              | 3.47 ± 0.83     | 5411                   | 2.2              | 1200              |      |
| 61  | WNe5-w       | WNe5-w        | 63.1              | 8.89 ± 2.85     | 5411                   | 2.3              | 1243              |      |
| 149 | (c) WNe5-s    | WNe5-s        | 63.1              | 5.20 ± 1.81     | 5411                   | 2.6              | 1181              |      |
| 129 | (c) WNe4-w    | WNe4-w        | 63.1              | 3.07 ± 1.33     | 4686                   | 6.3              | 1639              |      |
|     |               | WNe4-w        |                   | 3.93 ± 1.57     | 5411                   | 2.4              | 1191              |      |
| 91  | (d) WNe7(WNE-s) | WNe7(WNE-s)   | 70.8              | 9.17 ± 0.92     | 4686                   | 8.2              | 2003              |      |
|     |               | WNe7(WNE-s)   |                   | 10.96 ± 1.92    | 5411                   | 2.4              | 1684              |      |
| 62  | (d) WNe6-s    | WNe6-s        | 70.8              | 3.04 ± 0.99     | 4686                   | 9.0              | 2353              |      |
|     |               | WNe6-s        |                   | 2.76 ± 1.11     | 5411                   | 2.6              | 2139              |      |
| 110 | WNe5-s       | WNe5-s        | 70.8              | 2.82 ± 1.07     | 4686                   | 7.4              | 3658              |      |
| 51  | (d) WNe4-w    | WNe4-w        | 70.8              | 1.95 ± 0.72     | 4686                   | 6.1              | 1648              |      |
|     |               | WNe4-w        |                   | 2.68 ± 1.23     | 5411                   | 2.1              | 1070              |      |
| 100 | (d) WNe7(WNE-s) | WNe7(WNE-s)   | 79.4              | 6.36 ± 2.37     | 5411                   | 2.2              | 1972              |      |
|     |               | WNe7(WNE-s)   |                   | 6.43 ± 2.31     | 5876                   | 2.1              | 2566              |      |
| 44  | WNe4-w       | WNe4-w        | 79.4              | 5.01 ± 2.53     | 5411                   | 2.2              | 1286              |      |
| 37  | WNe4-s       | WNe4-s        | 100               | 3.17 ± 1.54     | 4686                   | 9.5              | 3000              |      |
|     |               | WNe4-s        |                   | 3.69 ± 1.40     | 5411                   | 2.5              | 2700              |      |
| 1   | WNe4-s       | WNe4-s        | 112.2             | 6.24 ± 1.11     | 4686                   | 8.9              | 2615              |      |
|     |               | WNe4-s        |                   | 9.19 ± 3.52     | 5411                   | 2.5              | 2364              |      |
| 7   | WNe4-s       | WNe4-s        | 112.2             | 1.34 ± 0.87     | 4686                   | 11.9             | 2059              |      |
|     |               | WNe4-s        |                   | 2.72 ± 0.96     | 5411                   | 3.1              | 1681              |      |
| 18  | WNe4-s       | WNe4-s        | 112.2             | <1.76           | 5411                   | 2.4              | 2916              |      |
| 2   | WNe2-w       | WNe2-w        | 141.3             | 0.60 ± 0.20     | 4686                   | 3.3              | 4294              |      |

Notes.

\(^{a}\) From Hamann et al. (2006).

\(^{b}\) Variations close to the detection threshold.

\(^{c}\) Shows CIR-like variations with published periods.

\(^{d}\) Shows CIR-like variations without published periods.

3.2. Error Sources and Uncertainties

The main challenge of this study is that we are using archival data originally planned for a different purpose. The spectra were designed for the search of large-scale lpvs that are easy to detect and measure when present on the top of virtually any mildly strong spectral emission line. This leads to a certain number of error sources that need tailored mitigation.

One main error source, which we can easily characterize, is the photon noise of the spectra. Indeed, the equation for the \(\sigma\) spectrum does not differentiate real variations from the noise. Consequently, \(\sigma\) is artificially high and diverges from the real lpv amplitude when the variation level is close to the noise level. With a signal-to-noise ratio (S/N) for the spectra between 70 and 100 in the continuum, the \(\sigma\) spectrum diverges when flux gets as low as \(\approx 2.5\) times the continuum or lower (though this value may be higher when the S/N is lower). This is the other of the two reasons (see above) why the \(\sigma\) value is calculated only within one FWHM of the emission line, since doing so respects this conditions in most of the cases.

Another issue occurs with very strong emissions lines that cannot be normalized with an accuracy better than 1% due to a lack of continuum over a large wavelength range. In those cases, the lpvs can be affected by a low frequency variation that artificially increases the \(\sigma\) value. This problem varies with the line intensity, the separation between the regions of continuum to the line, and the complexity of the continuum shape.
Table 4

| WR | Group | Spectral Type | $T_{\text{eff}}$ (kK) | $\sigma$ (%) | sp. Line He II\(\lambda\) | Line int. ($F_{\text{cont}}$) | Line FWHM (km s\(^{-1}\)) | Note |
|----|-------|--------------|----------------------|-------------|--------------------------|-----------------------------|-----------------------------|------|
| 79a | (a)   | WN9h        | 35.5                 | $<1.52$     | 5411                     | 1.0                         | 140                         |      |
| 79b | (a)   | WN9h        | 35.5                 | $<1.44$     | 5411                     | 1.0                         | 101                         |      |
| 108 |       | WN9h        | 39.8                 | $<1.48$     | 4686                     | 2.1                         | 381                         |      |
| 156 |       | WN8h        | 39.8                 | 4.27 ± 1.06 | 4686                     | 3.3                         | 419                         |      |
| 124 | (b)   | WN8h        | 44.7                 | 4.18 ± 1.25 | 4686                     | 3.7                         | 689                         |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 158 | (b)   | WN7h+Be?    | 44.7                 | 3.93 ± 0.80 | 4686                     | 3.2                         | 657                         |      |
| 87  |       | WN7h        | 44.7                 | $<1.16$     | 5411                     | 1.2                         | 343                         |      |
| 131 |       | WN7h        | 44.7                 | 2.18 ± 1.04 | 4686                     | 3.2                         | 803                         |      |
| 85  | (c)   | WN6h-w(WNL) | 50.1                 | 3.73 ± 1.10 | 5411                     | 2.0                         | 728                         |      |
| 78  | (c)   | WN7h        | 50.1                 | $<1.39$     | 5411                     | 7.6                         | 126                         |      |
| 20b | (c)   | WN6ha       | 50.1                 | 2.46 ± 0.95 | 4686                     | 3.3                         | 1412                        |      |
| 24  | (d)   | WN6ha-w(WNL)| 50.1                 | $<1.57$     | 5411                     | 1.2                         | 601                         |      |
| 28  | (d)   | WN6h-w      | 50.1                 | $<1.91$     | 5411                     | 1.6                         | 600                         |      |
| 82  | (e)   | WN7(h)      | 56.2                 | 3.40 ± 1.21 | 4686                     | 1.2                         | 1026                        |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 35  | (e)   | WN6h-w      | 56.2                 | 1.89 ± 0.75 | 4686                     | 7.0                         | 1117                        |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 45  | c     | WN5o        | 63.1                 | 1.99 ± 0.87 | 4686                     | 7.5                         | 1707                        |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 10  | (f)   | WN5ha-w     | 63.1                 | $<2.44$     | 5411                     | 2.3                         | 1223                        |      |
| 136 | (g)   | WN6(h)-s    | 70.8                 | 1.53 ± 0.64 | 4686                     | 12.0                        | 2027                        |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 128 | (g)   | WN4(h)-w    | 70.8                 | 2.06 ± 0.87 | 4686                     | 4.3                         | 1742                        |      |
|      |       |             |                      |             |                          |                             |                             |      |
| 152 |       | WN3(h)-w    | 79.4                 | 2.87 ± 0.46 | 4686                     | 4.1                         | 1772                        |      |
| 7   |       | WN3h-w      | 89.1                 | 2.06 ± 0.48 | 4686                     | 2.4                         | 1742                        |      |

Notes.

a From Hamann et al. (2006).
b Variations close to the detection threshold.

Table 5

| WR | Group | Spectral Type | $T_{\text{eff}}$ (kK) | $\sigma$ (%) | sp. Line He II\(\lambda\) | Line int. ($F_{\text{cont}}$) | Line FWHM (km s\(^{-1}\)) | Note |
|----|-------|--------------|----------------------|-------------|--------------------------|-----------------------------|-----------------------------|------|
| 88 | WC9/WN8 | 40           | 5.81 ± 1.66          | 5696        | 7.7                      | 1018                        |                             |      |
|    |       |              |                      |             |                          |                             |                             |      |
| 126 | WC5/WN  | 63           | 1.72 ± 0.55          | 4686        | 3.1                      | 2734                        |                             |      |
|    |       |              |                      |             |                          |                             |                             |      |
| 8  | WN7o/CE | 79           | 5.68 ± 1.47          | 5411        | 2.1                      | 1115                        |                             |      |
|    |       |              |                      |             |                          |                             |                             |      |
| 26 | WN7/WCE | 79           | 4.98 ± 0.76          | 5411        | 2.3                      | 3005                        |                             |      |
| 58 | WN4/WCE | 79           | 4.05 ± 1.95          | 5411        | 3.0                      | 1800                        |                             |      |

Note.

a From Hamann et al. (2006) and Sander et al. (2012).

Finally, time sampling also contributes to the uncertainties.

(dominated by the spectrograph’s illumination profile). We avoid those lines as much as we can.

In some cases, spectra continuum is variable due to an external source (e.g., a potential binary companion or stray light in the instrument). For those stars, the lines were normalized to a uniform intensity, assuming that the clump variability would be sufficiently unaffected by variations taking place over a broad wavelength range.
the \( \sigma \) spectrum may end up lower and more skewed than it would be with better sampling. One remedy to these setbacks would be to define the \( \sigma \) value as the maximum value of the \( \sigma \) spectrum. But because \( \sigma \) may be overly influenced by noise, and because there would be no way to assess a statistically significant uncertainty on the value, such an approach would introduce additional systematics, and is not recommended. Instead, we opt for the median value, which is more robust.

We define the error on \( \sigma \) as the standard deviation of the \( \sigma \) spectrum within the wavelength range used to calculate \( \sigma \). This may not correspond to the standard definition of error bars, but it does represent the effect of our limited time sampling well. If there are no better lines than those affected by the continuum normalization issue, we add 1\% to the final error budget on \( \sigma \). Finally, if only faint spectral lines were available for a given star, and the noise level was close to the amplitude of the lpv, we considered the lpv as not detected, and used the detection threshold defined by the TVS as the maximum value possible. The errors are typically around 1\%, or less when the S/N atop the line is high. The error is a few tenths of a percent for WR 2 and WR 142, as \( \sim 70 \) spectra where used instead of four to five. The same would apply to WR 102 if variability was detected.

3.3. \( \sigma \) Dependence on Spectral Line

Ideally, the same spectral line would be used for all the stars to measure \( \sigma \). And the best candidates would be He II\( \lambda \lambda 4686 \) for WN stars and C III\( \lambda \lambda 5696 \) for WC stars, as they are both singlets originating at large radii in the wind. However, this was not possible for two reasons. The first one is the different wavelength range covered during the multiple observing campaigns that produced the data we are using. The second, inevitably, is the dependence of the spectral lines intensity with the temperature (or spectral type).

Our analysis is therefore based on the assumption that the \( \sigma \) calculated for a given line is statistically equivalent to the value calculated for any other line. This assumption was verified by Chené & St-Louis (2011), when different spectral lines than for St-Louis et al. (2009) were used. Indeed, the results for WR 111 and WR 115 were the same regardless of which spectral lines were studied. Chené & St-Louis (2010) also plot the \( \sigma \) spectrum for WR 1 for nine lines, which did not all give the exact same value, but differences were below 1\% (for lines that are not affected by any of the issues mentioned above), comparable to the error bars. On the other hand (Lépine et al. 2000), observations of WR 135 show that the C IV\( \lambda \lambda 5808 \) doublet region gives a systematically lower \( \sigma \) than other lines in that case.

To make sure our assumption is valid, we analyzed as many spectral lines per star as we could use, making sure to use only the best line, as free as possible from systematic issues. Looking at Tables 2–5, we find that the difference in \( \sigma \) between lines is always within the error, but with a few exceptions. In some cases, one of the line intensities is close to the limit at which noise contributes to \( \sigma \) significantly, potentially causing the associated \( \sigma \) to be over evaluated. More importantly, the C IV\( \lambda \lambda 5808 \) doublet region is effectively systematically less variable for WC7 and WC8 stars. We suspect that at their temperature, the contribution of the two components of the line’s doublet nature blends the variations and falsely create lower amplitude residuals. We therefore avoid using that line for those stars.

4. Line Profile Variability of WR 2, WR 102, and WR 142

In this section, we present the observed lppv of the three WR stars that we are adding to the sample, WR 2, WR 102, and WR 142. The lppv are illustrated in Figures 2–4, respectively. The residuals created by subtracting the mean spectrum from individual spectra are shown in the grayscale plots. The \( \Sigma \) spectrum is presented in the bottom panel.

4.1. WR 2

The wavelength range only allows for the monitoring of the He II\( \lambda \lambda 4686 \) line changes. All other lines observed have a lower intensity, and our spectra at those wavelengths do not reach an S/N high enough for a significant detection of low amplitude lpv.
Each series observed during the first three epochs (plotted on the left side of Figure 2) contains 11 spectra and covers ∼45 minutes. Even in these short data sets, one can clearly see rapidly moving subpeaks on top of the line, indicating that clumps are present in WR 2’s wind. However, the contiguous time-span is not long enough to monitor individual subpeaks from the moment they appear to the moment they dissipate. Luckily, we obtained a fourth series that covers a total of ∼2.6 hr (middle of Figure 2). Due to adverse weather conditions, the series was cut into two 1.2 hr series, the second of which was obtained using an exposure time of 250 s (slightly more than twice as long as for the previous spectra), to compensate for the absorption caused by passing clouds.

The TVS (calculated for the four nights all together) shows that the He II λ4686 line is variable over the whole wavelength range covered by the line. The detected lpv is well above the threshold where the variations are significant at the 99% confidence level, as defined by the TVS. All the subpeaks move toward the wings of the line and never cross the central wavelength, as expected for systematic clump motion following the general wind expansion. Hence, clumps are definitely detected in the wind of WR 2.

One interesting result is that the variability extends well above the terminal velocity found by Shenar et al. (2014) of $v_{\infty} = 1800$ km s$^{-1}$. A model of WR 2 briefly presented in Chené et al. (2019), yielded a terminal velocity of $v_{\infty} = 3200$ km s$^{-1}$, closer to this value and matching older spectral analysis from Schmutz et al. (1989). We therefore suggest that the wind of WR 2 reaches a much higher terminal velocity than previously thought.

A measure of the standard deviation of the intensity variations at each wavelength (as presented by St-Louis et al. 2009, for other WR stars) indicates that the subpeaks have an average rms of 0.6% of the line intensity, which is half the amplitude observed in the WR winds showing the smallest clump-like variations in the study of Robert (1992). This explains why clumping was not detected in WR 2 in previous data sets with lower S/Ns.

### 4.2. WR 102

We monitored the lpv of three of the WR 102 strongest emission lines, i.e., the C III/IV λ4659 multiplex, the O VI λ5290 line, and the C IV λ5808 doublet region. Our five sequences of ∼45 minutes each obtained during different nights do not seem to reveal any significant variability (see Figure 3). The TVS is far below the threshold where the variations are significant at the 99% confidence level, even on top of the strong C III/IV λ4659 multiplex.

One could be more or less convinced by looking at Figure 3 that some consistent structures could be seen traveling on top
of the lines. WR 102 ($V \sim 14.1$ mag) is fainter than WR 2 and WR 142 and was observed under the worst weather conditions; thus, it is possible that its S/N was insufficient for detecting clumps. We therefore use the S/N on top of the C III/IV $\lambda$4659 multiplex to determine the maximum amplitude limit clumps should have (in percent of the line’s intensity) to be at the same level as the noise in our data. This value is 0.14% of the line intensity.

4.3. WR 142

We monitored the lpvs of the same three lines of WR 142 as for WR 102. During the first two 45 minute long runs, we could see faint subpeaks moving on top of all the emission lines. We therefore used all the remaining observing time of our program to obtain a 2 hr long continuous monitoring. The clumps are barely visible and the trajectory of the subpeaks are traced only with difficulty. But the TVS confirms that we get a significant level of variability that is of comparable amplitude as the noise itself. We therefore interpret this as a significant detection of clumps with an amplitude equal to the noise level on top of the C III/IV $\lambda$4659 multiplex, which converts to an amplitude of 0.12% of the line intensity.

5. lpv Dependence on Surface Temperature

New improved $\sigma$ values for 90 WR stars, now including three extremely hot WR stars with $\sigma$ values determined to 0.1% accuracy (due to the larger number of high-S/N spectra used), allow us to reexamine the possible relationship between the amplitude of the variability due to clumping and the temperature at the hydrostatic stellar surface (Figure 5), as first presented by Michaux et al. (2014).

The top panel of Figure 5 presents our results in the form of log($\sigma$) as a function of $T_*$ (at the hydrostatic stellar surface, obtained by spectroscopic modeling from Hamann et al. 2006 and Sander et al. 2012) for stars of types limited to WC and WO. The $\sigma$ values obtained from different lines are plotted in different shades of blue. Overall, there is a significant decline of the lpv amplitude as a function of $T_*$. Assuming a linear association between log($\sigma$) and $T_*$, the fitted slope is $-(9.0 \pm 2.0) \times 10^{-6}$ K$^{-1}$. In this case, the Pearson correlation coefficient $r = -0.85$ and the permutation test gives a $p$-value essentially equal to 0, which supports the hypothesis of a linear association. The dispersion of the $\sigma$ values at a given temperature may appear high, and to be consistent with a slope, WR 143 and WR 144 should have clumps about half the amplitude measured. But the overall rms dispersion of the data is comparable to the rms error on the $\sigma$ values, and the observations of the spectral lines for both WR 143 and WR 144 were affected by the continuum normalization issues. Indeed, the spectrum of those two WC 4 stars consists of many weak lines with few very intense lines that are tens of times the intensity of the continuum. Because our observing strategy was not well prepared for that, the best we could do was to get a rough estimate of the $\sigma$ value from one line that offered the best compromise. A project dedicated to those two stars and to WR 52, which was not observed with sufficient S/N, would be necessary to verify if the clumps reach an amplitude of 1% or less in WC winds with temperatures around 100 kK. Nevertheless, whether the trend is an exponential relationship or a more complex relationship, the lpv in the winds of the cool
In that case, either the stochastic lpv is larger at 100 kK, or both stars do have CIRs in their winds. A dedicated project to search for periods in those two stars, and to also reobserve WR 18 for which we could only determine an upper limit, would help settle this question.

The bottom panel shows only the WN stars with H lines in their spectra. These stars appear to follow a similar trend as the WN stars without H (here plotted with two dotted–dashed lines), although possibly at a slightly lower level overall.

Note here that an equally good relation is obtained using a log-log plot. In such a case, the slopes are $-2.3 \pm 0.2$ for WC/O stars $-2.03 \pm 0.2$ for WN stars without H. The Pearson correlation coefficients are $r = -0.85$ and $r = -0.79$, respectively, and the $p$-values are essentially equal to 0.

Finally, one could wonder if the trend with temperature could be impacted by not using the same spectral lines to calculate $\sigma$ for all the stars of the same spectral type. As mentioned in Section 3.3, there is a difference between the $\sigma$ values obtained using C III and C IV lines for the WC7 and WC8 stars. Yet that difference is merely 1% at most, while the trend we present shows a deviation bigger than one order of magnitude between the coolest to the hottest stars’ $\sigma$ values.

6. Interpretation

If the lpv amplitude observed in WR winds is correlated with the surface temperature of the star, what does it tell us about the origin of the clumps? Unfortunately, there is currently no way to know precisely where exactly lpvs come from. Is one bump associated with one clump, or a group of clumps? Is the lpv pattern on one spectrum a snapshot of the density distribution of the clumps in the wind, or are they dominated by clumps that are the densest and/or the biggest? Consequently, we cannot easily link the $\sigma$ value, which is a measure of the amplitude of the lpvs, to a specific physical parameter of the clumps. On the other hand, it is safe to assume that it is representative of a certain level of clumpiness in the wind. One possible objection to this assumption is that the amplitude of the variations in the line profile could be dominated by narrow lpvs, but with high amplitude, while wider and lower amplitude ones would not contribute as much, even with the same total flux. Yet, there are two reasons this objection does not apply. The first comes from the way we calculate $\sigma$: a narrow and high amplitude lpv would give a comparable value to that of a wider and lower amplitude lpv, once averaged over the wavelength range of the line and would only give larger error bars. The second reason, which is even stronger, is that in fact lpvs with high amplitude tend also to be wider, while lower amplitude lpvs tend to be narrower, as illustrated in Chené & St-Louis (2011).

A priori, the dependence of the level of clumpiness, represented by the lpv’s amplitude, is in contradiction with concluding that the LDI is the sole origin of clumps. But does that disqualify it totally? In this section, we explore the possible ways to explain the observed trend, as there are a few competing ideas that can possibly explain a reduction in the variability of clumping at higher (hydrostatic surface) temperature.

6.1. Reduced LDI with Temperature

Starting with the density, $\rho = \dot{M} / (4\pi R^2 v_\infty)$, where $\dot{M}$ is the mass-loss rate, and $v_\infty$, the wind’s terminal velocity, if we take...
\( R_* \) as the hydrostatic radius, we can rewrite:

\[
\rho = \frac{\dot{M} \sigma T_4^4}{(L \nu_\infty)},
\]

(1)

where \( T_* \) is the stellar temperature at the hydrostatic surface, \( L \) is the luminosity, and \( \sigma \) the Stefan–Boltzmann constant. Also, \( \tau_0 = n_0 R_* \sigma T \), where \( \sigma \) the Thompson’s constant, we can develop \( n_0 \), the number density and get:

\[
\tau_0 = \frac{M R_* \sigma T^4}{L \nu_\infty \mu_e m_H},
\]

(2)

where \( m_H \) is the mass of the hydrogen atom, and \( \mu_e = 2 \) for pure once ionized helium. We consider only the hydrostatic surface, because it is where clumps are expected to be formed, and where the wind is anchored. Following Equations (1) and (2), a hotter star will be more compact, with a denser, more optically thick wind where the continuum is emitted, with every other stellar parameter being kept the same. Optical depth effects can reduce the level of LDI: indeed, the linear growth rate is inversely proportional to the effective optical depth (in the sense of the number of overlapping optically thick lines over a terminal speed). The usual growth rate is the ratio of the terminal speed to the ion thermal speed per flow time, so if one divides that ratio by the number of thick lines per terminal speed, one finds that the number of \( e^{-folds} \) of the instability is of the order of the ratio of \( c \) to the ion Doppler width (so perhaps 30,000) divided by the number of optically thick lines over the entire spectrum. So to completely suppress the LDI, it would require many thousands of optically thick lines. The effective optical depth also gives the ratio of the wind momentum flux to \( L/c \), which would need to be many factors of 10 in order to kill the LDI. But it is (barely) possible to do this with very dense winds close to the Eddington limit as in WR stars. In Figure 6, we plot the \( \sigma \) value as a function of the \( e^{-folds} \) (from Gayley & Owocki 1995):

\[
e^{-folds} = 70 \sqrt{\frac{M}{40 M_\odot}} \sqrt{\frac{T}{40 \text{kK}}} \left( \frac{L}{5 \times 10^5 L_\odot} \right)^{-1/4} P^{-9/8},
\]

(3)

where \( P \) is the wind momentum flow divided by \( L/c \):

\[
P = \frac{M v_\infty c}{L}.
\]

(4)

From that figure, there certainly does not appear to be any obvious dependence of sigma on \( e^{-fold} \). There are outliers in \( e^{-fold} \), which tend to be outliers in \( \sigma \) as well, but in the wrong sense to the one required to be explained by LDI. We therefore consider the reduction of LDI with temperature as less likely.

In some sense, there has always been a problem explaining clumping with the LDI alone. The LDI and the \( e^{-fold} \) calculation only apply over length scales smaller than the Sobolev length, which is about \( R_\odot (v_D / v_\infty) \), where \( v_D \) is the Doppler width of the driving lines, and this is perhaps 1% of the stellar radius. It is therefore a double-edged sword—the number of \( e^{-folds} \) is high, since the length scale is small, but that produces a lot of tiny features, and lots of them. Increasing the value of \( P \) does not change the length scale, but does reduce the \( e^{-folds} \), which should reduce the value \( \sigma \). However, it would probably not be a slow trend and there would be a critical value of \( P \) where the instability would shut off. There is no evidence of any critical \( P \) in our data.

6.2. The Partial Ionization Zone

If the LDI does not by itself succeed in explaining this data set (and clumping in general), as proposed at the beginning of this paper, a better accounting for the trends in the data could be given by interpreting the \( \sigma \) value as being increased by an SSC zone, which becomes deeper at high \( T_* \), as expected. The stars with the weakest-\( \sigma \), WR 2, 102, and 142, could still be consistent with the expectations of a raw LDI without surface stirring by an SSC, but they can also be regarded as the low-\( \sigma \) tail of dying SSC effects. There is also good evidence that the strongest-\( \sigma \) stars require an additional process, beyond an SSC: when variations are proven to be periodic, they are related to stellar spots and/or pulsation and the way rotation can organize large-scale surface features into globally clumped features like CIRs.

In that interpretation, convection is necessary to stir the surface, and the nonlinearities of line driving yield a visible clumping effect. Convection by itself is not very efficient on wind speed scales, but line driving is notoriously good at producing denser structures out of small inhomogeneities. Furthermore, there is a distinction to make between the LDI, which is a local instability within the wind and only operates on small scales (smaller than the Sobolev length), and the basic line-driven nonlinearities, which appear even in the Sobolev approximation (and therefore operate on scales much larger than the Sobolev length). From a basic line-driven nonlinearity, any enhancement of the wind density and/or velocity by some 10% somewhere near the critical point, where the steady mass-loss rate is set would lead to a significantly larger than 10% effect on the wind density and/or velocity later on farther out in the wind. In other words, surface variations get leveraged by their effect on the local mass flux, and time dependence at the surface breaks the steady-state condition and can produce much larger time dependence in the wind. Therefore, if an SSC is causing clumping, it is not doing so by itself, but that can still...
be distinguished from the LDI (which might operate on a scale too small to be detectable in optical spectra).

6.3. Terminal Velocity

Before concluding this section, we wish to point out that our interpretations assume that the $\sigma$ value varies with the surface temperature. But a comparison of the temperatures, $T_*$, with the terminal velocities, $v_{\infty}$, determined by Hamann et al. (2006) and Sander et al. (2012), shows that they are correlated. Unfortunately, $v_{\infty}$ is not determined as accurately as $T_*$, yet for higher $T_*$, winds are faster. Depending on how the turbulence is generated at the base of the wind and carried away in the wind, one can expect many plausible different density profiles. Because the models currently available fail to describe how parameters commonly used to determine clumping, such as the filling factor, $f$, in atmospheric models, or the vorocity, introduced by Owocki (2008), which refers to the porosity in the wind induced by spatial variations in velocity, depend on $v_{\infty}$ or $T_*$, there is currently no clear path for exploring how our observations could be used to test the theory. All we can say for the moment is if the relation of $\sigma$ with $v_{\infty}$, it would be in contradiction with any predictions made based on LDI only, as hotter and faster should in that context show a higher level of clump-related variability.

7. Conclusions

We determined the amplitude of the lpvvs for the stars WR 2, 102, and 142 within 0.1%. We also revisited the $\sigma$ values (with a $\sim 1\%$ accuracy) and their relation to the surface temperature, $T_*$ (or $v_{\infty}$), presented in Michaux et al. (2014). In addition to confirming higher $\sigma$ values for cooler WR stars ($T_* \lesssim 50$ kK), we show that hot WR stars ($T_* \gtrsim 100$ kK) show $\sigma$ values much lower than the average.

Figure 5 shows an apparent linear relation between $\log(\sigma)$ and $T_*$. The quality of the data does not allow us to determine if that association represents a strict exponential relationship, which could help explore further the nature of the mechanism at the origin of the clumps, neither can we claim the presence of any significant knee in the relationship.

Our preferred theory for the origin of clumps is the presence of a PIZ causing an SSC, which in turn creates perturbations at the base of the wind that are amplified later by LDI. For higher surface temperature, the PIZ gets closer to the surface. The closer to the surface the SSC is, the lower the energy it can inject at the base of the wind. One could imagine that above a certain temperature, the PIZ is not present and there are no SSC perturbations at the base of the wind. Yet, there is nothing in this study supporting the possibility of this extreme case.

Of course, we recognize that more theoretical work can be required to settle this question. In the meantime, we plan to improve the determination of the dependence of clumping on the surface temperature, and dedicate observing campaigns on monitoring the clumps in WR 37, 7, 18, 144, and 143. These stars are the very few in the intermediate temperature range between 100 and 120 kK, where the expected $\sigma$ should be around or slightly lower than 1% of the line amplitude.

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