STACKING-BASED DEEP NEURAL NETWORK: DEEP ANALYTIC NETWORK ON CONVOLUTIONAL SPECTRAL HISTOGRAM FEATURES

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ABSTRACT

Stacking-based deep neural network (S-DNN), in general, denotes a deep neural network (DNN) resemblance in terms of its very deep, feedforward network architecture. The typical S-DNN aggregates a variable number of individual learning modules in series to assemble a DNN-alike alternative to the targeted object recognition tasks. This work likewise conceives an S-DNN instantiation, dubbed deep analytic network (DAN), on top of the spectral histogram (SH) features. The DAN learning principle relies on ridge regression, and some key DNN constituents, specifically, rectified linear unit, fine-tuning, and normalization. The DAN aptitude is scrutinized on three repositories of varying domains, including FERET (faces), MNIST (handwritten digits), and CIFAR10 (natural objects). The empirical results unveil that DAN escalates the SH baseline performance over a sufficiently deep layer.

Index Terms—Deep analytic network, face recognition, object recognition, multi-fold filter convolution, spectral histogram

1. INTRODUCTION

Stacked generalization (SG) [1], in addition to bagging and boosting [2], was devised as a means of aggregating shallow learning models into composite one to improve the predictive force. The generic SG is of 2-level stacked-up architecture, where the level-1 input receives either the level-0 predictions (along with its true class labels), or the level-0 class probabilities, and the least-square linear regression is adopted as the level-1 generalizer for the classification tasks at hand. Some initial SG works are [1], [3] and [4].

The earliest stacking-based deep neural network (S-DNN), i.e., the cascade-correlation learning architecture [5], surfaced about the same time with SG. The latter S-DNNs, e.g., [6] and [7], primarily emphasize on the sequential labeling tasks. Other relatively modern S-DNNs are the deep neural network (DNN)-motivated exemplars, specifically, the deep belief network (DBN) [8], the deep Boltzmann machine (DBM) [9], and the deep autoencoder (DAE) [10], etc. One might assert that each of the restricted Boltzmann machine (RBM)-learned weight sets in DBN, as an example, would be globally fine-tuned via back-propagation like what DNNs do. The DBN network basis, however, still relies on the stack-up principle. Although a full understanding for S-DNN is somehow elusive (since there is still no theoretical foundation), the key intuition is that S-DNN decipher a large scale problem via modularization. Each S-DNN module, either be a sub-network, or merely an interleaved layer with non-linearity, learns an effective function individually to be stacked up in a chain, with the output of one feeding the input of the next. As there is no interaction in between modules, each module is engaged to a pre-fixed problem, and learns to resolve that problem decisively and independently. Of course, the S-DNN learning speed is considerably faster than DNN as it necessitates no back-propagation.

One of the inspiring exertions in the recent S-DNN literature is the deep convex network (DCN) [11]. Each DCN module indicates a specialized single hidden layer network yielding a ridge regression output set to the immediately adjacent module. The DCN innovation is extended to the kernel-DCN (K-DCN) [12], and K-DCN is further revised to tackle its scalability problem via random Fourier features for Gaussian kernel approximation [13]. The S-DNN closest to DCN include the deep extreme learning machine (D-ELM) variants, e.g., the stacked ELM (S-ELM) and the autoencoder-based stacked ELM (AE-S-ELM) [14], the hierarchical-ELM (H-ELM) [15], etc. If the input-hidden weights of DCN are randomly set, it is generalized to the one equipping a series of ELMs. Other works delineated under this umbrella term are [16], [17], [18], etc.

This paper outlines a parsimonious S-DNN alternative to DCN, S-ELM, AE-S-ELM, and other counterparts, coined as deep analytic network (DAN) henceforth. The unique traits of DAN are: (i) DAN replaces the plurality of the layer-wise non-linear projections, either using random weights (as in S-ELM), or learnable weight sets, e.g., RBM-learned weights (as in DCN) and autoencoder-learned weights (as in AE-S-ELM), with the filter-based spectral histogram (SH) features [19]; (ii) the key DNN constituents, i.e., rectified linear unit (ReLU), proper fine-tuning, and normalization, are absorbed into the DAN pipeline; and (iii) our goal is not to compete with DNNs, but rather scrutinizing the extent to which the SH baseline performance is advanced via the stacking-based DAN. The 2-stage DAN framework is portrayed in Fig. 1 as unsupervised, convolutional SH feature extraction in the first stage, followed by supervised, fully-connected DAN. Other details pertinent to DAN will be unveiled in the subsequent sections.

2. SPECTRAL HISTOGRAM FEATURES

The SH features are in line with DNN from the convolutional feature extraction perspective. The SH techniques, as a whole, pursue three stages: (i) a single-flat, or two-layer filter-image convolutions, either based on the learning-free Gabor filters, discrete Cosine transform (DCT) filters, etc., or the pre-learned filter ensembles, e.g., principal component analysis (PCA) filters, independent component analysis (ICA) filters, etc.; (ii) a non-linearity, i.e., binarization, followed by local binary pattern (LBP)-alike feature encoding; and (iii) a feature pooling stage via block-wise histogramming. The recent SH efforts include, but not limited to, binarized statistical image feature (BSIF) [20], PCA network (PCANet) [16], two-fold filter convolution (2-FFC) [21], etc. This work, however, only adopts the BSIF, PCANet, and 2-FFC features as the DAN principal input to be post-appended with the layer-wise regression outputs.

3. DEEP ANALYTIC NETWORK

Similar to DCN and the D-ELM variants, DAN learns based on the long-existing ridge regression [22]. The primary reason leading us
This implies that the negative regression outputs in \( \mathcal{F} \) can be re-written as:

In other words, \( \mathcal{F} \) receives \( \psi \) to be biased owing to \( \gamma \), and are therefore zeroed. In contrast to the modular fine-tuning (FT) practiced in DCN, the DAN FT layer, serving as the DAN output layer, synthesizes \( q_{\ell} \) into \( \mathcal{W}^{(\text{FT})} \) to learn \( \mathcal{W}^{(\text{FT})} \in \mathbb{R}^{P_{\ell} \times C} \) as follows:

In fact, the RR-based FT layer is parallel to the last DNN softmax layer. Depending on the task difficulties, it is opted to other classifiers such as support vector machines (SVM).

### 4. EXPERIMENTAL RESULTS AND DISCUSSION

We access DAN with \( L = 10 \) layers in the primal, or the dual form, depending on \( N, D_{\ell} \), and \( D^{(\text{FT})} \). The DAN learning aptitude over the 10 layers is analyzed on three image classification tasks: (i) FERET FA, and 4 probe sets with facial expression, illumination and time-related disturbances, i.e., FB, FC, DUP I, and DUP II. The FERET images are realigned with respect to the annotated eye coordinates and are each rescaled into 128x128 images. (ii) MNIST [24] consists of 70,000 gray-scale handwritten digits of each 28x28 pixels, where 60,000 images are for training and the rest for testing; (iii) CIFAR10 [25], on the other hand, possesses a sum of 60,000 natural images in each of 70,000 gray-scale handwritten digits of each 28x28 pixels.
RGB, with each 32×32×3 pixels. The training and testing sets are of 50,000 and 10,000 images, respectively. No other manipulation is applied, and also our experiments involve no data augmentation. The BSIF, PCANet and 2-FFC features are abstracted beforehand based on the parameters configured in the respective papers, unless stated otherwise. The baseline performance evaluated on the original SH features is estimated using the naive nearest neighbor classifier with the Cosine similarity scores. For result replicability, the DAN hyper-parameters for each dataset is summarized in Table II. These parameters are fine-tuned as a whole across \( \mathcal{L} \) layers.

Table I. DAN step-by-step learning procedures.

| Step | Procedure |
|------|-----------|
| 1    | If \( \ell = 1 \), \( H_1 = F \). |
| 2    | Otherwise, \( H_{\ell} = \{ H_{\ell-1}, \ldots, q_{\ell-1} \} \in \mathbb{R}^{N \times D_{\ell}} \), where \( D_{\ell} = d + C(\ell - 1) \), and \( \ell = 2, \ldots, \mathcal{L} \). |
| 3    | \( \tilde{W}_{\ell} \in \mathbb{R}^{D_{\ell} \times C} \) with respect to (6). |
| 4    | \( q_{\ell} = \max(0, p_{\ell}) \), where \( p_{\ell} = H_{\ell} \times \tilde{W}_{\ell} \in \mathbb{R}^{N \times C} \). |
| 5    | Compute \( W_{(\ell)} \in \mathbb{R}^{N \times D_{\ell}} \) with respect to (7). |

Table II. DAN hyper-parameter configuration with respect to varying datasets.

| Parameter | Feret | MNIST | CIFAR10 |
|-----------|-------|-------|---------|
| \( \lambda_{1, \ldots, \mathcal{L}} \) | 0.1   | 10    | 10      |
| \( \lambda^{(FT)}_{1, \ldots, \mathcal{L}} \) | 0.1   | 10    | 10      |
| \( \beta \) | 0.5   | 0.6   | 0.6     |

4.1. Performance Analysis

The DAN pipeline is decomposed into 4 instances to scrutinize its layer-wise learning aptitude benefitted from the very deep stacked-up building blocks, and the absorbed DNN essentials, i.e., ReLU and FT: (i) with no ReLU and no FT, i.e., linear DAN; (ii) with FT only, i.e., linear DAN with FT; (iii) with ReLU only; and (iv) with ReLU and FT. We observe from Table III that, for the 10-layer DAN with the original 2-FFC features, the linear setting fails to trigger DAN to learn after first layer - the rank-1 recognition rate is capped at 94% on the FERET DUP II probe set. If the linear DAN is affixed with a RR-based FT layer, its performance is progressed from the minima of 44.02% to 95.30%. To recap, the FT layer only accepts the power-normalized regression outputs \( Q \) as the inputs, without the 2-FFCPCA features (refer to Section 3). In other words, for the single-flat layer DAN, the FT layer is forced to learn from the injudicious \( q_{1} \), leading to a drastic performance drop. For the DAN with a sufficient depth, the \( \mathcal{L} \) stacked-up regression outputs, i.e., \( q_{1}, \ldots, q_{\mathcal{L}} \) in this case, are evidenced yielding meaningful features for the FT output layer. The DAN with only ReLU, like what the linear DAN experiences, shows no improvement after the first layer. This is due to the reason that \( Q \) suffers from the disparity problem to be regularized via the power-normalization in the FT layer. We attest in our experiments that both ReLU and the FT output layer are of indispensable. The DAN with these two DNN absorptions escalates the baseline performance from 83.76% to 97.01%.

Table III. Performance summary, in terms of rank-1 identification rate (%), for DAN of depth 10 using 2-FFCPCA on FERET DUP II probe set.

| DESCR. | DUP II |
|--------|--------|
| 2-FFCPCA | 83.76  |

4.2. Performance Evaluation on FERET

To our knowledge, there is no S-DNN relevant works evaluating on FERET, except PCANet. We thus only compare the performance of DAN to that of K-DCN [12], where each K-DCN module is, in fact, a kernelized-ELM. Table IV reveals that, with DAN or K-DCN, the baseline performance is vastly intensified across the FERET probe sets, particularly for the PCANet, and 2-FFCPCA features. The DAN performance, on average, stands out over K-DCN. We discern that, for the relatively less discriminative features like BSIF, the K-DCN learnability immediately comes to a halt right after the first layer. In contrast, DAN continues learning as it deepens into the succeeding layers. Note that, we derive the BSIF features with respect to only 8 natural image-learned ICA filters shared by the authors. We believe that the DAN performance in FERET is the best in the recent face recognition literature.

4.3. Performance Evaluation on MNIST

In addition to S-ELM and AE-S-ELM [14], the convolutional DBN (CDBN) [26], DBM [9], and the stacked denoising autoencoders (SDAE) [10] are compared in Table V. With the adoption of the SH features, DAN, by contrast, outshines the remaining marginally. It is noteworthy that both S-ELM and AE-S-ELM demands a deeper network to be outstanding in performance. It is logged in the paper that S-ELM and AE are respectively built with 650 and 700 in depth; while the finest DAN performance is attainable in the 7-th layer with 99.34% for the PCANet features, and the 8-th layer with 99.45% for the 2-FFCPCA features. In accordance with1, the least generalization

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1 http://rodrigob.github.io/are_we_there_yet/build/
error on MNIST to date is of 0.21%, equivalent to 99.79%, achieved by the regularization of neural network (R-NN) [27]. We notice that R-NN augments the training images to learn 5 networks, where the final concluding performance is decided via voting. However, its accuracy is voted to be 99.43%, similar to that of DAN, without data augmentation.

Table IV. Performance summary, in terms of rank-1 identification rate (%), for DAN and K-DCN based on the BSIF, PCANet, and 2-FFCPCA features onFERET. The DAN and K-DCN layer yielding the best performance is superscripted in parentheses.

| DESCRIPTOR | FB | FC | DUPS I | DUPS II | MEAN |
|------------|----|----|--------|---------|------|
| BSIF [20]  | 93.47 | 69.07 | 71.75 | 59.40 | 73.42 |
| BSIF + K-DCN | 99.25 (1) | 98.97 (1) | 87.67 (1) | 85.47 (1) | 92.84 |
| BSIF + DAN | 99.58 (6) | 100 (2) | 92.66 (7) | 89.74 (7) | 95.50 |
| PCANet [16] | 94.73 | 96.04 | 86.72 | 98.30 | 91.49 |
| PCANet + K-DCN | 97.75 (4) | 100 (1) | 96.82 (4) | 95.30 (2) | 97.97 |
| PCANet + DAN | 99.75 (2) | 100 (1) | 97.92 (4) | 96.15 (2) | 98.46 |
| 2-FFCPCA [21] | 95.65 | 99.48 | 86.57 | 83.76 | 91.36 |
| 2-FFCPCA + K-DCN | 99.75 (4) | 100 (1) | 96.82 (4) | 95.30 (2) | 97.97 |
| 2-FFCPCA + DAN | 99.83 (2) | 100 (1) | 97.92 (4) | 97.01 (3) | 98.69 |

Table V. Performance summary, in terms of rank-1 identification rate (%), for DAN and other relevant counterparts on MNIST probe set, where * denotes the empirical results reported in the respective papers.

| DESCRIPTOR | MNIST |
|------------|-------|
| PCANet      | 98.81 |
| PCANet + DAN | 99.34 (7) |
| 2-FFCPCA    | 99.01 |
| 2-FFCPCA + DAN | 99.45 (4) |

4.4. Performance Evaluation on CIFAR10

The CIFAR10 images are of relatively more challenging compared to those in FERET and MNIST (due to wide intra-class variations). The PCANet features are replicated with 40 spatial pyramid pooling (SPP) histogram features [28] in $4 \times 4$, $2 \times 2$, and $1 \times 1$ sub-regions. In the meantime, with the 2-FFC elasticity, we derive the composite SPP features, dubbed 2-FFC_COMP in this section, with respect to the 2-FFC PCA filters, the 2-FFC ICA filters, and the 2-FFC PCA-ICA filters. To closely approximate the PCANet features, the 2-FFC_COMP features are loaded with 39 SPP histograms, i.e., 13 for each 2-FFC offspring type, in the same sub-region grids.

In place of the RR-based FT, the linear SVM classifier with the penalty parameter $C = 10$ is plugged into the DAN output layer to adapt DAN in a generally more complicated task. Table VI discloses that the SVM-based DAN with the PCA-compressed (due to overly long features) PCANet and 2-FFC_COMP features of 5000 dimensions improves the baseline performance by at least 13%. Besides that, we also examine DAN against feature fusion for additional performance gain. The concatenated PCANet and 2-FFC_COMP features (refers to the row of $A + B$ in Table VI) further rises the accuracy to 79.30% in the 3-th DAN layer.

For reference, the CIFAR10 official portal\(^2\) underlines that the DNN standard performance with and without data augmentation are of 89% and 82%, respectively; the 3 top-ranked DNNs summarized in Table I achieves 96.53% for fractional max-pooling network (FMP-Net) [29], 95.59% for large all convolutional network (large ALL-CNN) [30], followed by 99.43% for layer-sequential unit-variance network (LSUV-Net) [31]. Note that, FMP-Net and LSUV-Net are renamed for self-explanatory convenience. The common grounds (in addition to the gradient descent-based training algorithms) are: (i) most of the DNNs learns a bag of networks; FMP-Net, as an example, involves 100 networks; (ii) aggressive data augmentation, as in FMP-Net, ALL-CNN, and LSUV-Net.

Table VI. Performance summary, in terms of rank-1 identification rate (%), for DAN and other relevant counterparts on CIFAR10 probe set, where * denotes the empirical results reported in the respective papers.

| DESCRIPTOR | CIFAR10 |
|------------|---------|
| PCANet + PCA 5000 | 63.52 |
| 2-FFCPCA + PCA 5000 | 61.92 |
| 2-FFCPCA + PCA 5000 + DAN | 76.27 (3) |
| 2-FFCPCA + PCA 5000 + DAN | 76.27 (3) |
| A + B | 79.30 (5) |

5. CONCLUSION

This work outlines a deep analytic network (DAN), i.e., a stacking-based deep neural network (S-DNN) instantiation, which simulates the typical feedforward deep neural network (DNN) in terms of its deep architecture. One of the distinguishable traits over DNN is that, the outputs for each S-DNN learning module are stacked up to one another as it traverses deep into the network. Unlike other S-DNNs, either relying on layer-wise non-linear random projection, or other learning-based projection, the DAN pipeline manipulates the filter-based spectral histogram features. The empirical results unveil that the DAN with an ample depth leads to remarkable performance gain compared to the corresponding baselines. To bridge the performance gap in between DAN and DNN, it will be revisited to cater other key DNN essentials, e.g., dropout, whitening normalization, global fine-tuning, to name just a few.

\(^2\) https://www.cs.toronto.edu/~kriz/cifar.html
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