Third-Generation Light-Driven Symmetric Molecular Motors

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Supporting Information

ABSTRACT: Symmetric molecular motors based on two overcrowded alkenes with a notable absence of a stereogenic center show potential to function as novel mechanical systems in the development of more advanced nanomachines offering controlled motion over surfaces. Elucidation of the key parameters and limitations of these third-generation motors is essential for the design of optimized molecular machines based on light-driven rotary motion. Herein we demonstrate the thermal and photochemical rotational behavior of a series of third-generation light-driven molecular motors. The steric hindrance of the core unit exerts a pivotal role in controlling the speed of rotation, where a smaller size results in lower barriers. The presence of a pseudo-asymmetric carbon center provides the motor with unidirectionality. Tuning of the steric effects of the substituents at the bridgehead for the precise control of the direction of disrotatory motion, illustrated by the design of two motors which show opposite rotation with respect to a methyl substituent. A third-generation molecular motor with the potential to be the fastest based on overcrowded alkenes to date was used to visualize the equal rate of rotation of both its rotor units. The autonomous rotational behavior perfectly followed the predicted model, setting the stage for more advanced motors for functional dynamic systems.

INTRODUCTION

Molecular motors and machines attract major attention, as the introduction of dynamic properties enables a wide range of responsive functions and adaptive properties in synthetic materials.1−6 Toward the design of dynamic functional systems, the use of light as an external stimulus offers particular advantages. Photochromic systems arguably have the benefit of non-invasive triggering with the potential of high spatial-temporal precision.7,8 Switching between two or more states upon irradiation at different wavelengths (UV/vis) can be combined with other effectors (temperature, pH, metal-ion binding, redox) to arrive at multiresponsive behavior.9,10 Prominent classes of photochemical switches include dithienylethenes, stilbenes, fulgides and fulgimides, spirophanes, DASA, or azobenzenes.11−13 Stilbenes in particular, though rather easy to prepare, suffer from the undesired thermal cis−trans isomerizing and degradation due to ring closing and oxidation toward phenanthrene (Figure 1a).14,15 One of the major interests in our group has been the synthetic manipulation of stilbenes in order to achieve stability and increase quantum yield, control over irradiation wavelengths, and directionality of motion upon isomerization, and furthermore structural modifications to prevent decomposition.16

An important synthetic adjustment of a stilbene-like system (Figure 1b) was achieved by Feringa and Wynberg, introducing steric overcrowding at the alkene to form thermally stable chiral forms. This was accomplished through the presence of naphthalene moieties and aliphatic rings at both sides of the central alkene to prevent ring closing.17 The introduction of stereogenic centers in these systems (Figure 1b) originally served the purpose of proving the absolute stereochemistry of its analogues.18 However, the molecules were found to have a surprising new property: they are able to undergo a 360° unidirectional rotation around the alkene bond.19 These systems, as a result of successive alterations, became the basis of the first-generation synthetic molecular motors, characterized by their C2 symmetry and its principal axis at the double bond connecting upper and lower halves. Recently, functional...
analogs of these first-generation synthetic motors showed potential in asymmetric catalysis\textsuperscript{26} and control of dynamic chirality\textsuperscript{27} and as chiral hosts.\textsuperscript{28}

In subsequent studies, one half of these new dynamic molecules was symmetrized in order to increase their speed and quantum yield as well as allowing surface assembly.\textsuperscript{29–31} Synthetic modifications were introduced to illustrate that these motors can perform work.\textsuperscript{32} The desymmetrized synthetic unidirectional motors with only one stereogenic center in the upper half and a symmetric lower half were adopted as second-generation molecular motors, in which chirality was shown essential to ensure unidirectionality. The initial “stilbene motive” is continually shown in orange in all four structures in order to illustrate the predominant concept of the isomerizing alkene connecting two aromatic groups, Figure 1b. Not surprisingly, the question regarding the necessity of a stereogenic center for unidirectionality in rotary motion emerged. Recently, we reported a novel synthetic meso motor bearing two overcrowded alkenes and the notable absence of a stereogenic center, although a pseudo-asymmetric center is present.\textsuperscript{33} In fact, each individual alkene still has to experience chirality in order to perform a unidirectional rotation. This so-called third-generation molecular motor (Figure 2) has two such alkene moieties with identical groups that can be considered mirror images of two separate second-generation motors. This third-generation motor is specially designed to maintain unidirectionality of two parallel rotors while avoiding the stereogenic element (asymmetric carbon center) known from earlier generations of motors. Both individual alkenes experience the pseudo-asymmetry of the bridge unit (e.g., CFCH\textsubscript{3} in 2), and, due to the opposite helicity of these alkenes with respect to the bridge unit, both fluorene moieties are rotating in the same direction with respect to the core aromatic group. This symmetry property is analogous to a car driver moving forward on a road observing his right wheel turning anti-clockwise and his left wheel turning clockwise.

Here, we report on our investigation and characterization of the essential features of third-generation molecular motors and the limits of their performance, to finally come to demonstrate the unidirectionality of the fastest third-generation motor and potentially the fastest of all molecular rotary motors based on overcrowded alkenes designed so far. We first identify the impact of the core’s size on its behavior by a computational study followed by an experimental verification. Based on those results, we study the effect of the size of the substituents at the pseudo-asymmetric carbon atom (the indane bridgehead C-2, Figure 2) on the behavior of the bis-overcrowded alkenes using theoretical and experimental approaches.\textsuperscript{34–38} After identifying the most desirable structural features, we choose a suitable candidate as a model compound for proving the persistence of unidirectionality in ultrafast third-generation molecular motors.

### RESULTS AND DISCUSSION

Previously, unidirectional rotation has been established for motor 2 taking advantage of its desymmetrized analogue 3.\textsuperscript{33} For purposes of developing more advanced nanomachines and controlled motion along surfaces, the ability to tune the rotary speed is considered highly beneficial.\textsuperscript{35,39} We therefore instigated a theoretical study on double overcrowded alkenes with a substitution pattern of two methyl groups on C-2 (R\textsubscript{1} = CH\textsubscript{3}) such as 4 for maximum simplicity. Besides 4, four more structural units were selected starting with a benzene instead of xylene moiety in the core (5), a p-difluorobenzene (6), a p-dimethoxybenzene (7), and one where the core xylene moiety is replaced with a phenanthrene moiety (8) (Chart 1).

Chart 1. Double Overcrowded Alkenes with Modified Core Moieties Featuring Benzene (5), p-Difluorobenzene (6), p-Dimethoxybenzene (7), and Phenanthrene (8)

![Figure 2. Schematic design of achiral motors. Merging of two enantiomers of motor 1 (opposite helicities (P,M) and central chirality (R,S) indicated) gives rise to symmetric double overcrowded alkenes 2–4 (pseudo-asymmetric carbon atom C-2 indicated with “2”).](image-url)

Theoretical Study of the Core-Size Effect: The theoretical investigation was performed using the semiempirical PM6 model to construct a potential energy surface (PES) from two dihedrals governing the aromatic planes for compounds 4–8 (4 as example; Figure 3a). The resulting PES shows a two-fold symmetry with mirror planes running diagonally through the minima. The geometries of the minima and transition states (TSs) were optimized using DFT B3LYP/6-31G(d,p)\textsuperscript{40,41} and intrinsic reaction coordinates (IRCs, 4 as example; Figure 3b) were calculated to ensure the TSs connected the identified minima. Subsequently the geometries of the minima and TSs were optimized using DFT \textit{ω}B97X-D/6-31+G(d,p)\textsuperscript{42} in dichloromethane (IEFPCM)\textsuperscript{43,44} which revealed for each compound two global minima and two metastable local minima (minima and TSs afforded zero or one imaginary frequency, respectively, and their geometries, energies and calculated barriers are shown in Table 1). The two redundant global minima have the desired meso geometries and are close to or have C\textsubscript{1} symmetry. The two metastable local minima were enantiomeric helical configurations and are close to or have C\textsubscript{2} symmetry and connected to the global minima by the calculated TSs which constitute the thermal helix inversions (THIs) known for overcrowded alkenes. The redundant global minima possess C\textsubscript{1} symmetry for 6 and 8 or deviate marginally from it by twisting the rotors in 4, 5,
and 7, although not detectible by NMR due to the minute barrier of isomerization (Cs symmetric geometries are 0−1.6 kJ·mol⁻¹ higher in energy, Table 1). A similar phenomenon is observed for the two metastable local minima in 4−7 which deviate slightly from C₂ symmetry by twisting one of the methyl groups on C-2 lowering the energy by 3−7 kJ·mol⁻¹. Again, this deviation from symmetry would not be observed by NMR since at room temperature the isomerization is very fast in which the averaged geometry is a C₂ symmetrical conformation. The isomerization pathway between the helical minimum and the global minimum (from now on referred to as C₂-x and Cs-x, respectively) showed increasing thermal barriers for helix inversion going from 5 < 6 < 7 < 8 which corresponds fully with the increase in size of the aromatic core moiety (Table 1). The temperature at which the half-life is 1 h (T at t₁/₂ = 1 h for THI C₂→Cs) is a good indication of which compound would be most suitable for an NMR study. This suggests that 5−7 require very low temperatures for NMR measurements, whereas both 8 and 4 are in a temperature region where measurements can be readily performed. The two redundant meso configurations (C₅-x and C₅-x') can interconvert through C₂-x by two helix inversions (2×THI, shown for 4 in Figure 3a). The barrier for this isomerization can be quantified from the approximate theoretical coalescence temperature of ¹H NMR resonances (CH₃ group resonances are calculated to be separated by ~10 Hz, vide infra). From the calculated coalescence temperatures (Table 1), compound 5 appears to be the only suitable candidate for NMR investigation. To investigate the THI and 2×THI processes, compounds 4 and 5 as well as 9 were synthesized (Scheme 1).

Table 1. Optimized Geometries of Minima and Transition States and Their Corresponding Gibbs Free Energies of 4−8, in kJ·mol⁻¹ (DFT ωB97X-D/6-31+G(d,p) in DCM)a

|          | 5       | 6       | 7       | 4       | 8       |
|----------|---------|---------|---------|---------|---------|
| global minimum (C₅)a | 0.0 (0.4) | 0.0 (0.0) | 0.0 (0.7) | 0.0 (1.6) | 0.0 (0.0) |
| helical minimum P/M (C₂)b | 41.3 (43.9) | 45.4 (50.5) | 46.1 (52.2) | 49.4 (56.3) | 29.5 (29.5) |
| transition state       | 66.9    | 96.0    | 107     | 123     | 132     |
| THI C₅→Cs, T at t₁/₂ = 1 h (°C) | −216   | −121   | −82.8   | −46.6   | 45.5    |
| 2×THI C₅→Cs, Tcoalescence (10 Hz) (°C)c | 44.0   | 182   | 234     | 310     | 353     |

aGeometries shown with methyl groups facing the reader, the H₃C−C−CH₃ bonds in the y−z plane, and the five-membered ring core in the x−z plane.
bEnergies in parentheses are for the symmetrical geometries.
cUsing $k = \pi \Delta \nu_0 x_0^{-1/2}$ to provide the rate at $T_{coalescence}$. $k$ can be used in combination with the calculated barriers to solve the Eyring equation for $T$. 

Figure 3. (a) PES of 4 (PM6, colored from 0 kJ·mol⁻¹ (red) to 150 kJ·mol⁻¹ (violet), x-axis: 1−2−3−4 dihedral (in °); y-axis: 5−6−7−8 dihedral (in °)), (b) IRCs of TS-4.
Derivative 9 was expected to have increased solubility compared with 5 and might provide insight into substituent effects for future functionalization.

Scheme 1. Synthesis of Compounds 4, 5, and 9

Experimental Study of Core Size. The synthesis of the core structure of overcrowded alkenes 4, 5, and 9 started with a double Friedel–Crafts acylation of dimethyl malonil chloride on p-xylene afforded the bis-ketone in high yield (82%). This was transformed into the bis-thioketone by the use of phosphorous pentasulfide (97%). A Barton−Kellogg coupling of the bis-thioketone and dazofluorene followed by a desulfurization by the use of hexamethylphosphine triamine (HMPT) yielded the desired double overcrowded alkene C-4 (17%). For compound 5, after double alkylation of indane-dione with methyl iodide, an analogous pathway was followed where phosphorous pentasulfide was used to afford the bis-thioketone. This indanedithione underwent a Barton−Kellogg coupling with dazofluorene to give the desired product C,-5 in good overall yield (50%). Double overcrowded alkene 9 caused problems in the first step, producing significant amounts of C-alkylated side-product which resulted in loss of product during purification, providing the C-alkylated product in 9% yield. The next two steps proceeded in an analogous fashion to the synthesis of 5 affording the desired C-9.

The study of the photochemical and thermal isomerizations started with compound 4, which was irradiated with UV light (365 nm in CH2Cl2, Figure 4a), and at room temperature no change was observed in the UV−vis absorption spectrum. Irradiation at −65 °C was accompanied by a bathochromic shift in the absorption-spectrum indicative of an increase in strain over the alkenes pointing to the formation of a metastable intermediate. After irradiation to the photostationary state (PSS), the sample was allowed to warm up to rt and full reversal to the original spectra was observed. Three cycles of irradiation at low temperature and heating at ambient temperatures did not reveal any signs of fatigue. During both of these processes an isosbestic point was observed at the same wavelength (459 nm), indicating the absence of side reactions during these first order reactions. 1H NMR confirmed the identity of the stable global minimum as C-4 by the presence of three distinct methyl resonances, which is expected of a C symmetry configuration, corresponding to C-4. Following low temperatures revealed the metastable state possessing a C symmetry configuration, corresponding to C-4. Following the integrals of the NMR-resonances of H over time at different temperatures enabled the construction of an Eyring plot (Figure 4c) which provided the energies of activation (ΔH° = 63.2 ± 1.6 kJ·mol−1, ΔS° = −17.3 ± 7.0 J·K−1·mol−1, ΔG° = 68.3 ± 0.5 kJ·mol−1, k1/2 = 1 h at T = −59.4 ± 0.3 °C) in reasonable agreement with the calculated barrier (ΔH°calc = 70.3 kJ·mol−1, ΔS°calc = −10.6 J·K−1·mol−1, ΔG°calc = 73.4 kJ·mol−1).

Figure 4. Thermal behavior of 4. (a) UV−vis absorption spectrum of C-4 in CH2Cl2 at rt, irradiation (365 nm, 30 min) to PSS at −65 °C and warming to rt (inset: isosbestic point at 459 nm with absorptions during both processes added). b) i. 1H NMR spectrum of C-4 (CD2Cl2, 500 MHz, rt), assignment in Scheme 1. ii: Transferred to a Shigemi tube and irradiated in NMR to PSS (CD2Cl2, 365 nm, 12 min, 600 MHz, −58 °C). iii: t = 30 min (CD2Cl2, 600 MHz, −58 °C). iv: t = 8 h (CD2Cl2, 600 MHz, −58 °C, x = impurity, presumably acetonitrile). c) Exponential decay curves of the normalized integrals of H over time (left and top axis) and Eyring plot with error bars of 3σ (right and bottom axis).
Irradiation of double alkene C₅ in n-pentane at −60 °C did not show any shift in the UV–vis absorption spectrum (see Supporting Information for the UV–vis spectrum) which indicates that either C₅ does not undergo a double bond isomerization or more likely the thermal barrier for reversion of C₅ to C₅ is too low to observe the metastable species at that temperature. The barrier for THI at room temperature was calculated to be 25.6 kJ·mol⁻¹ (vide supra) which would allow for a lifetime of 2 ns at −60 °C and a temperature of −215 °C would be required to allow for a lifetime of 1 h. Due to the low barrier for THI, C₅ is not expected to be observed over the experimental temperature range. Photocyclization has been a problem for an overcrowded alkene without functional groups in the fjord region; however, no photocyclization was observed in the case of compound 5 probably due to insufficient π-orbital overlap. Moreover, no other photochemistry was observed, such as described for 1,2-distyrylbenzene derivatives, likely due to the rigid cyclopentane. An NMR study confirms the identity of the stable global minimum C₅ by the presence of two distinct methyl resonances, which is expected of a C₅ symmetrical conformation of 5 but not of C₅. This is corroborated by the calculated ¹H NMR spectrum of C₅ (DFT giao mPW1PW91/6-311+G(2d,p) in CHCl₃) which strongly agrees with the experimental spectrum (Figure 5).

Low temperature UV–vis and NMR displayed a similar absence of change under irradiation and, similar to C₅, presence of C₅ symmetry for compound 9 was shown by NMR (Figure 5; see Supporting Information for UV–vis and ¹³C NMR spectra). An interesting pattern was observed for the ¹H NMR resonances of the alkyl chains of C₅. The first methylene on each alkyl displayed a similar significant downfield shift like the methyl groups of C₅, but here the strongest shift was observed for the pseudo-axial methylene group (H₁₁) instead of the pseudo-equatorial methyl in C₅ (H₀). Due to their distinct chemical environments, the two different alkyl chains follow a peculiar pattern with methylene groups of the equatorial alkyl chain exhibiting large upfield shifts. A theoretical study of several rotamers of the alkyl chains of C₅ and calculation of their average ¹H NMR spectrum provided a strong agreement with the experimental spectrum (R² = 0.999, Figure 5, see Supporting Information for details). Increasing the temperature caused coalescence of the alkyl groups most apparent for the resonances of H₁₁–H₁₂ at ~2.7 ppm. This allowed for the determination of the barrier for thermal isomerization (Δ²G = 59.4 ± 1.0 kJ·mol⁻¹) which again is lower than the computed barrier (Δ²G⁰(calc) = 65.7 kJ·mol⁻¹, Δ²H⁰(calc) = 51.7 kJ·mol⁻¹).

Conclusive information on the configuration of 9 came from X-ray crystallography. Crystals suitable for X-ray diffraction studies were grown by layered diffusion of a concentrated solution of 9 in dichloromethane on top of which volumes of, successively, pentane, heptane, and methanol were layered. The structure determination shows that there are two independent molecules in the unit cell (Figure 6; see Supporting Information for complete unit cell), which have similar metrical parameters. Both have approximate C₅ symmetry (meso configuration) around the core of the bis-overcrowded alkene 9. The alkyl group in the equatorial position is in both cases rotated such that the last three C-atoms of the hexyl chain are located directly above the plane of the fluorene ring, with C₅hexyl–fluorene distances of 3.577–4.073 Å. This conformation of the equatorial alkyl group agrees with its anomalous upfield shift observed in the ¹H NMR spectrum. It is unclear, however, whether this folding in the solid state is due to packing effects or represents a genuine attractive interaction (see Supporting Information for a computational conformational study).

Figure 5. Temperature-dependent experimental and calculated ¹H NMR spectra of C₅ and C₅.

Figure 6. Molecular structure of C₅ by crystallography (only one of the two independent molecules is shown).

Upon an increase in temperature, coalescence of the methyl resonances is observed, indicative of the two-step process in which the Me₀ (H₁₁) and Meₐ (H₁₂) exchange environment through a double helix inversion. The barrier determined by NMR (Δ²G = 62.5 ± 1.0 kJ·mol⁻¹) is found to be lower than the computed barrier (Δ²G⁰(calc) = 66.9 kJ·mol⁻¹, vide supra), probably due to a deviation in the calculated entropy term as was observed for 4. However, it still suggests that at these temperatures the redundant isomers C₅ and C₅ exchange through thermal processes as shown for 4 in Figure 3a.

To investigate these processes in greater detail compound 9 (Scheme 1) has been synthesized which is expected to show behavior similar to 5 but with a significantly increased solubility.
Conclusions on the Influence of Core Size. Molecular motors based on double overcrowded alkenes with a benzene moiety in the core show the potential to be significantly faster than those with a substituted benzene group. However, compounds 4–9 with C₈ symmetrical stable meso states do not possess a preference for either of the two redundant geometries and therefore no preference for which of the two states undergoes a photochemical E–Z (PEZ) isomerization. The metastable helical states possess C₄ symmetry and therefore both rotors show an equal probability for undergoing a THI. Due to the redundancy of the stable states and the C₄ symmetry of the metastable state these rotors do not prefer a specific direction and are therefore not unidirectional. On account of the symmetry of the stable state it is expected that a PEZ isomerization of C₈-9 will produce a photostationary state (PSS) between C₈-9 and racemic C₈-9 (Figure 7). This isomerization yields a rotation of one of the rotors on C₈-9 and a rotation of one of the rotors on C₈-9', in opposite direction with respect to C₈-9. The metastable C₈-9 undergoes a THI of either of the rotors without preference because its C₄ symmetry as indicated in Figure 7, producing equal amounts of C₈-9 and C₈-9'. Over two rotational steps (PEZ–THI) the rotations sum up to a net rotation of zero due to the lack of unidirectionality. This behavior is expected for all compounds with equally sized substituents at the bridgehead position such as 4 and 5. To achieve unidirectional rotation, a form of asymmetry has to be reintroduced like in 2 and 3, which is achieved by substituting two differently sized moieties at the indane bridgehead (carbon 2, Chart 1) making it a pseudo-asymmetric carbon atom.

Theoretical Study of the Substituent Effect. Several substitution patterns on the indane bridgehead were considered and investigated computationally. Certain stERICally interesting substituents such as tert-butyl (large) and hydrogen and methoxy (smaller than methyl) were disregarded on account of their synthetic demand and the expected chemically unstable nature of the resulting double overcrowded alkenes. Note that for instance compound 2 (R₁ = H, Figure 2), featuring a hydrogen in a double allylic position can readily undergo 1,3-H-shift removing the pseudo-asymmetric center. After initial calculations on multiple double overcrowded alkenes (DFT B3LYP/6-31G(dp)) five were selected (18–22) and studied in depth (DFT ωB97X-D/6-31+G(dp) in DCM, Table 2). For an additional side-view perspective of the meso geometries of 18–22 as well as the calculated enthalpies, see the Supporting Information.

The three possible combinations of a methyl, an alkyl, and a phenyl group (compounds 18–20) were selected because of their interesting potential balance in steric effects. Both the phenyl and the alkyl moieties have been reported to be slightly or significantly larger than the methyl group, though there are instances in which the methyl group has been reported to exhibit a similar or larger steric effect. The sterically demanding isopropyl group (compound 21) and small fluorine atom (compound 22) were selected to realize the largest difference in steric effect with respect to a methyl group. For each compound four minima were calculated, similar to 4–8 (vide supra), of which two were the enantiomeric helical metastable forms and two were found to represent the stable meso isomers with either an r or s configuration at the pseudo-asymmetric carbon atom. Note that, similar to 4–7 (vide supra, Table 1), the calculated minima geometries for r-18–22 and s-18–22 deviate slightly from true C₄ symmetry by small twists of substituents or rotors, as can be clearly observed for s-18 and r-21. As before, this is not expected to be detectible by NMR due to the low barrier of isomerization which goes through the true C₄ symmetrical geometry (energies shown in parentheses in Table 2).

For motors 2 and 3 it was shown that the larger substituent prefers a pseudo-axial orientation, with the rotor moieties pinching the substituent in the pseudo-equatorial orientation. The change from a xylene core as in 4 to a benzene core in 5 increases the pinching effect of the rotors (Table 1), and the preference for the larger substituent to adopt the pseudo-axial orientation is therefore expected to remain present. To exemplify, in r-18, r-19, r-21 and r-22 the pseudo-axial orientation is occupied by the methyl group. The larger substituents in 21 and 22 are the isopropyl group and the methyl group, respectively, and calculations show a preference for these groups to adopt the pseudo-axial orientation with s-21 and r-22 being lower in energy than their corresponding diastereomer (Table 2). The calculations presented in Table 2 also show a preference for r-18, r-19 and s-20 over their corresponding diastereomer, which suggest the following order for steric effects in these molecules: Me > Ph > alkyl.

The barriers for THI of metastable P/M-18–22 are calculated to be very low (19.1, 27.7, 21.6, 50.2, and 167 kJ·mol⁻¹, respectively), which makes a PEZ–THI sequence difficult to detect by conventional UV–vis or NMR techniques. The barrier for THI for 21 might be the highest for these overcrowded alkenes, although it would still require a temperature of −113 °C to obtain a half-life of 1 h. The calculated barrier of metastable P/M-22 to r-22 predicts it to be the fastest molecular motor to date with an expected half-life of only 109 ps at room temperature. The barriers for the double inversion of s-18–22 to r-18–22 or vice versa are calculated to be measurable by coalescence in H NMR (62.9, 66.6, 66.7, 72.1, and 51.2 kJ·mol⁻¹) on the condition that both
diastereomers are observed. The NMR spectra of \( \text{r-}18\sim22 \) and \( \text{s-}18\sim22 \) were calculated (DFT mPW1PW91/6-311+G(2d,p) in CHCl\(_3\)) in order to be able to assign the

**Table 2. Structures and Optimized Geometries of Minima and Transition States and Their Corresponding Gibbs Free Energies of 18–22 (DFT \( \omega \)B97X-D/6-31+G(d,p) in DCM)**

|    | 18 (Cs) | 19 (Cs) | 20 (Cs) | 21 (Cs) | 22 (Cs) |
|----|---------|---------|---------|---------|---------|
| r  | (10.6)  | (10.6)  | (12.5)  | (12.5)  | (12.5)  |
| s  | (19.1)  | (9.1)   | (0.0)   | (15.5)  | (0.1)   |
| helical minima P/M (C\(_1\)) | 48.3 | 42.0 | 39.0 | 28.6 | 37.4 |
| TS, P/M→r | 67.4 | 63.5 | 66.7 | 78.9 | 54.2 |
| TS, P/M→s | 74.5 | 75.6 | 71.6 | 78.8 | 67.4 |

\( ^{a} \)Structures shown in experimentally determined most stable isomer with numbers indicating \(^1\)H NMR assignments. Geometries shown with substituents facing the reader, the \( \text{R} \sim \text{C} \sim \text{R} \) bond in the \( y \sim z \) plane, and the five-membered ring core in the \( x \sim z \) plane. Alkyl chains of the geometries of \( 18 \) and \( 20 \) cropped to three carbons for clarity. Energies in kJ mol\(^{-1}\); energies in parentheses for the \( C\(_i\) \) geometries.

**Figure 8.** \(^1\)H NMR spectra of 18–22. Top: calculated spectrum of the \( r \)-isomer. Middle: calculated spectrum of the \( s \)-isomer. Bottom: experimental spectrum (CDCl\(_3\)) with numbering (see Table 2 for the assignments). Bottom right: correlation of experimental and calculated \(^1\)H NMR chemical shifts.
condensation of dimethyl phthalate and symmetric ketones with the aid of sodium hydride affords the monosubstituted indanediones 10–12 in accordance with the reported literature procedures. The second alkylation using alkyl halides on the indanediones gave rise to significant amounts of O-alkylated side products. This was suppressed by the use of phase transfer reagents, such as Aliquat 336, as well as the addition of potassium fluoride immobilized on Celite to the reaction mixture. The combination of both reagents afforded the highest yield and the best C:O-alkylated product ratio of 13–16, which was finally further improved on using cesium carbonate instead of potassium carbonate. The fluorinated indanedione 17 was obtained from methyl-indanedione using Selectfluor. Bi-functionalized indanediones 13–17 were transformed to the corresponding indanedithiones using phosphorus pentasulfide (or a combination with Lawesson’s reagent, see experimental section for details) of which most products appeared to be rather stable, probably due to a lack of hydrogens at alpha carbons. Nonetheless, the indanedithiones were directly submitted to double Barton–Kellogg couplings with diazo-fluorene to afford the desired double overcrowded alkenes 18–22 (Scheme 2).

The $^1$H NMR spectra of 18–22 were compared to the calculated spectra and were found to be in close agreement (Figure 8). It revealed 18–20 to be present in both isomeric forms ($r$- and $s$-isomers) while 21 and 22 were only found as a single isomer. At room temperature compounds 18–20 displayed coalescence of several resonances, though at low temperature (−30 °C) the compounds entered the slow exchange region and clearly resolved $^1$H NMR spectra were obtained. Using several 2D NMR techniques allowed for a complete proton and carbon assignment of the major isomers (see Supporting Information for all NMR spectra). The isomers of compound 18 were found in a 3.0:1:0 ratio of which the minor isomer displayed a similar effect for the hexyl chain as was observed for the pseudo-equatorially oriented hexyl chain in 9. This suggests the minor isomer to be $r$-18 and therefore $s$-18 to be the major isomer, which was confirmed by the comparison of the calculated $^1$H NMR spectra to the experimental one. In this comparison, the $s$ isomer strongly correlates to the major isomer of 18 and the $r$ isomer correlates to the minor isomer. The presence of coalescence was predicted by calculations, however, the asymmetry in the isomer ratio makes the use of the coalescence temperature as a tool to determine the barrier for isomerization of double helix inversion slightly unreliable. Therefore, we made use of temperature dependent 1D EXSY NMR to determine the activation parameters for the exchange process (Figure 9, Table 3).

**Scheme 2. Synthesis of Third-Generation Molecular Motors 18–22**

![Scheme 2](image)

$^{1}$Reagents and conditions: (i) NaH, toluene, 16 h, rt 10: 63%; 11: 31%; 12: 87%; (ii) K$_2$CO$_3$, Aliquat 336, KF on Celite, acetonitrile, reflux, 16 h, 13: 36%; 14: 83%; 15: 36%; 16: 84%; (iii) Selectfluor, 96%; (iv) P$_2$S$_5$, Lawesson’s reagent, toluene, 8–16 h; (v) 9-diazo-9H-fluorene, toluene, rt–reflux, 2–24 h, 18: 66%; 19: 23%; 20: 24%; 21: 3%; 22: 14% (over iv and v).

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**Figure 9. EXSY NMR of 18. (a) NOESY 1D $^1$H NMR spectrum of 18 (600 MHz, CDCl$_3$, –3.3 °C, 2 s mixing time). (b) Normalized integral of r−s at various mixing times and temperatures.**

**Table 3. Gibbs Free Energies of 18–20 for r−s Isomerization by EXSY NMR**

|       | 18   | 19   | 20   |
|-------|------|------|------|
| r→s  | $\Delta G^°/\text{kJ mol}^{-1}$ | 60.1 ± 0.3 | 62.3 ± 0.3 | 63.1 ± 1.1 |
| s→r  | $\Delta G^°/\text{kJ mol}^{-1}$ | 62.0 ± 0.3 | 63.4 ± 0.2 | 67.3 ± 1.1 |
| r→r′ | $\Delta G'^°/\text{kJ mol}^{-1}$ | 1.9 ± 0.3 | 1.0 ± 0.1 | 4.0 ± 0.2 |

*Standard state: atmospheric pressure and rt (20 °C).*
free to rotate making the hydrogens ortho and meta to the indane bridgehead chemically identical, while in the minor isomer the orientation of the phenyl is fixed giving rise to five different resonances. In r-19 the phenyl is in a pseudo-equatorial orientation, placing it in between the fluorene moieties (see the geometries in Table 2 and the Supporting Information), whereas in s-19 it is oriented pseudo-axially, giving it much more spatial freedom. This suggests the assignment of the major isomer being s-19 which corresponds fully with the calculated NMR spectra in which this assignment shows a far stronger correlation than the opposite combination does. EXSY NMR was again employed to determine the activation parameters for the double THI exchange process between the s and r isomers using the same method as was used for 18 (Table 3, see Supporting Information for NOESY 1D spectra and traces), revealing a similar barrier of 63.4 kJ mol\(^{-1}\) for the isomerization of the major isomer s-19 to the minor isomer r-19.

The isomers of compound 20 were found in an 8.9:1.1 ratio and for its aromatic region a nearly identical pattern is observed as was for 19, while for the aliphatic region a similar effect is seen in the exchange of a methyl group to an alkyl as was for 5 and 9 (Figure 8). In both 5 and 19, the pseudo-axial methyl group is shifted upfield with respect to the pseudo-equatorially oriented methyl group, while in both 9 and 20 the first methylene on the pseudo-axial alkyl group shows a downfield shift with respect to the pseudo-equatorial position.\(^{53}\) With again a good correlation of the calculated spectra to the experimental \(^1\)H NMR spectrum, the major isomer is assigned as s-20 and the minor as r-20. EXSY NMR revealed a barrier of 67.3 kJ mol\(^{-1}\) for the double THI exchange process going from the major isomer s-20 to the minor isomer r-20 (Table 3; see Supporting Information for NOESY 1D spectra and traces).

Considering the performance of overcrowded alkenes 18−20 as molecular motors, one should note that these systems feature reduced unidirectionality due to the presence of both isomers. Nonetheless, they still maintain preferential directionality of their rotary motion. For example, in 20 89% rotates in one direction (counterclockwise when observed from the left in Figure 8) while 11% rotates in the opposite direction resulting in a reduced unidirectional yield of 78% (determined from the r-20: s-20 ratio at rt, vide supra). This is not an issue in 21 and 22 since they were obtained as single isomers according to \(^1\)H NMR (Figure 8; note that the two resonances in the aliphatic group is shifted up\(^{9}\) than for\(^{9}\) the alkyl group \((\text{s-rt } \Delta G^\circ = 0.9, 3.2, \text{ and } 4.3 \text{ kJ mol}^{-1}\)) for the double THI exchange process going from the major isomer s-20 to the minor isomer r-20 (Table 3; see Supporting Information for NOESY 1D spectra and traces).

To obtain additional information on the structure and stereochemistry of the double overcrowded alkenes, crystals suitable for X-ray diffraction analysis were grown by layer diffusion of concentrated solutions of 19, 20, and 22 in dichloromethane on top of which volumes of, successively, pentane, heptane, and methanol were layered (from 18 and 21 no suitable crystals were obtained). The structure determination confirmed the expected meso configuration of the bis-overcrowded alkenes, moreover, 19 and 20 were both only found with an s configuration at the pseudo-asymmetric carbon atom (Figure 10). While this clearly shows a preference for both compounds to crystallize in a single configuration, it should not be used as independent proof for the assignment of the major isomer in solution since either isomer could have possessed a stronger tendency toward crystallization. However, NMR indicates only a single isomer of 22 to be present, and its X-ray analysis confirmed the computational prediction and NMR assignment, by showing 22 to possess an r configuration on the pseudo-asymmetric carbon atom (Figure 11).

![Figure 10. Molecular structures of s-19 and s-20 by crystallography.](Image 10)

Conclusions on the Influence of Substituent Size. The combined data shows the following order for steric effects of the substituents at the indane bridgehead in 18−22: i-Pr > Ph > alkyl > Me > F. However, just based on the data for 19 and 20 (Table 3) one might expect the methyl group to be larger than the alkyl group \((s-\text{rt } \Delta G^\circ \text{ being smaller for } 19 \text{ than for } 20\) highlighting the very subtle interplay of these steric moieties with the rest of the molecule. It is also clear that this deviates from the calculated order, which predicted the steric effect of the methyl group to be larger than those of the phenyl and alkyl groups \((\text{vide supra})\). The calculated barriers for the double THI exchange process of s-18−20 to r-18−20 agree well with the experimental barriers \((\Delta \Delta^2 G^\circ = 0.9, 3.2, \text{ and } 4.3 \text{ kJ mol}^{-1}\), Tables 2 and 3) while the agreement in the opposite process of r-18−20 to s-18−20 is much weaker \((\Delta \Delta^2 G^\circ = 14.4, 13.3, \text{ and } 4.0 \text{ kJ mol}^{-1}\), Tables 2 and 3). To improve the correspondence between theory and experiment it might be necessary to employ different functionals, add diffuse functions or increase the basis set. The combined experimental data also confirms that in the third-generation molecular motors s-21 and r-22 opposite directions of rotation take place while both possess a >95% unidirectional yield (since the opposite diastereomer is not observed in \(^1\)H NMR). As expected, no changes are observed in the NMR resonances at high or low temperature, or after irradiation at room or low temperature. This is due to the very low barrier for THI in combination with the symmetry of the rotors. In order to prove that these fast third-generation molecular motors are able to undergo rotation of the fluorene units under photo-irradiation, asymmetry has to be introduced in the rotor units.
Rotation of an Ultrafast Third-Generation Motor. To unequivocally demonstrate the unidirectional rotary motion, methoxy substituents were introduced in the rotor parts of the ultrafast motor with a benzene moiety as its core. Using methoxy-diazofluorene and the indanedithione of 17 in a Barton−Kellogg coupling (as in Scheme 2) afforded the desired desymmetrized double overcrowded alkene 23 as a statistical mixture of the four isomers (isomers shown in Scheme 3, for synthetic scheme see Supporting Information). This mixture was subjected to supercritical fluid chromatography (SFC) (45% 2-propanol in CO$_2$, Chiralpak ID at 3.5 mL·min$^{-1}$, 40 °C, 160 bar) which allowed the isolation of each isomer (Figure 12, isomers sequentially numbered and corresponding to the configurations numbered in Scheme 3). The four isomers are indistinguishable by UV−vis as can be seen from their nearly identical UV−vis absorption spectra (Figure 12). However, $^{19}$F and $^1$H NMR allowed for the assignment of the individual isomers where the enantiomers of 23 (isomers 1 and 3) displayed identical NMR spectra and were assigned based on their retention time in analogy to 3. Irradiation of an isolated isomer of 23 is expected to allow it to undergo a PEZ isomerization to be directly followed by a THI. This produces the two connected isomers according to Scheme 3 in an approximate 50:50 ratio, which go on to produce both the starting isomer as well as the final isomer connected to those isomers again in a 50:50 ratio. Finally, this last isomer is formed but at the same time undergoes isomerization producing the two intermediate isomers again. The rates presented in the kinetic scheme (Scheme 3) are formulated in rate equations which were solved using matrix methods, providing the following integrated rate laws (see Supporting Information for derivation and expanded formulas):

\[
([R,Z,E]-23)_t = ([R,Z,E]-23)_0 + A_1 e^{-k_1 t} + A_2 e^{-k_2 t} + A_3 e^{-(k_1-k_2)t} + A_4 e^{-k_4 t} + A_5 e^{-(k_1-k_4)t}
\]

(1)

\[
([r,E,E]-23)_t = ([r,E,E]-23)_0 + B_1 e^{-k_1 t} + B_2 e^{-k_2 t} + B_3 e^{-k_3 t} + B_4 e^{-k_4 t} + B_5 e^{-(k_1-k_4)t} + B_6 e^{-(k_1-k_3)t} + B_7 e^{-(k_1-k_2)t}
\]

(2)

\[
([S,Z,E]-23)_t = ([S,Z,E]-23)_0 + C_1 e^{-k_1 t} + C_2 e^{-k_2 t} + C_3 e^{-k_3 t} + C_4 e^{-k_4 t} + C_5 e^{-(k_1-k_2)t} + C_6 e^{-(k_1-k_3)t} + C_7 e^{-(k_1-k_4)t}
\]

(3)

\[
([r,Z,Z]-23)_t = ([r,Z,Z]-23)_0 + D_1 e^{-k_1 t} + D_2 e^{-k_2 t} + D_3 e^{-k_3 t} + D_4 e^{-k_4 t} + D_5 e^{-(k_1-k_2)t} + D_6 e^{-(k_1-k_3)t} + D_7 e^{-(k_1-k_4)t} + D_8 e^{-(k_1-k_5)t}
\]

(4)

where $[X]_t$ describes the final concentration, $k_V$ and $k_W$ are compiled rate factors including $k_1$−$k_4$, $A_1$−$D_4$ are compiled pre-exponential factors (including $[X]_0$ and $k_1$−$k_4$), and $t$ is time.

Concentrated solutions in CH$_2$Cl$_2$ of the individual isomers 1−4 of 23 purged with argon were placed in the autosampler of the SFC machine, in front of which a UV lamp (365 nm) was positioned. A high concentration was used to allow the sampling to be only 4 μL, to keep the change in total volume as small as possible, and simultaneously ensuring the process lasts long enough for the collection of sufficient data. While the samples were being irradiated, aliquots for SFC analysis were taken at regular intervals, the chromatograms were integrated, and the normalized integrals were plotted against time (Figure 13).

In Figure 13 the black curves are eqs 1−4 fitted against the experimental data points by least-squares analysis in a single fit providing a small residual error and a high coefficient of

![Figure 12. SFC chromatogram of 23 and the corresponding UV−vis, $^{19}$F NMR, and $^1$H NMR spectra of the individual isomers 1−4, with the numbering corresponding to the isomers shown in Scheme 3 (UV−vis spectra are offset for clarity).](image-url)
determination \( R^2 = 0.997 \); see Supporting Information for details of fitting). The observed behavior agrees with the proposed rate laws and proves the hypothesized connectivity as displayed in the rotational cycle in Scheme 3. Starting from any isomer of 23 there is an exponential decay of the initial isomer coupled with exponential formation of the two isomers directly connected to it, while the isomer across from the initial isomer experiences a delayed formation resulting in S-shaped curves (Figure 13). Starting from the meso isomers of 23 (isomers 2 and 4) there is no preference for either of the connected isomers, expressed in nearly identical formation curves of the two enantiomERIC isomers of 23 (isomers 1 and 3), while starting from one of the enantiomers, a small preference appears to exist for the formation of isomer 2 over isomer 4. This is expressed in a deviation from the final ratios from a simple statistical 1:1:1:1 ratio to a ratio of 0.99:1.1:0.99:0.90 (for isomer 1:2:3:4) starting from any of the isomers. Isomers 1 and 3 of 23 are expected to behave identically on account of their enantiomERIC relationship and therefore result in identical final ratios.

All experiments result in isomer 2 \([r(E,E)-23]\) as the major isomer and isomer 4 \([r(Z,Z)-23]\) as the minor isomer (this relationship is confirmed by an \(^1\text{H} \) NMR study, see Supporting Information for details). The origin of this behavior is two-fold: (i) enantiomERIC isomers 1 and 3 both slightly favor rotation of one rotor over the other by 2\% (normalized rates \( k_1 = 1.02 \) and \( k_2 = 0.98 \)), likely due to isomers 1 and 3 being chiral and therefore possessing an asymmetric PES in the excited state, and (ii) the rate of rotation is 8\% smaller for isomer 2 with respect to isomer 4 (normalized rates \( k_3 = 0.91 \) and \( k_4 = 1.08 \)) leading to an accumulation of isomer 2, which could be caused by a higher quantum yield of isomer 4 with respect to isomer 2. Nonetheless, no matter what the origin of this small deviation from statistical is, it would not play a role in the third-generation motors 21 and 22 with symmetric rotors. With the use of compound 23 it is shown that, even though the thermal step is too fast to be measured in a conventional way, these motors still undergo light-driven rotation and studies using ultrafast spectroscopy to identify the metastable states and quantify the barriers involved are currently ongoing.

**CONCLUSIONS**

We have demonstrated the thermal and photochemical rotational behavior of a series of third-generation light-driven molecular motors. The steric hindrance around the core proved to be decisive in the tuning of the potential speed of double-overcrowded alkenes. Computational prediction of \(^1\text{H} \) NMR spectra was used to support the assignment of experimental spectra as well as the relative configurations. The presence of a pseudo-asymmetric center has been shown to be essential to achieve unidirectional rotation. Careful modification of the steric bulk of the substituents on the bridgehead allows for the precise control over the direction of rotation, as clearly illustrated by the opposite directionality with respect to the methyl substituent taking place in motors 21 and 22. Motor 22 has the potential to be the fastest unidirectional motor based on overcrowded alkenes to date, and its desymmetrization into motor 23 allowed for the visualization of the equal rate of rotation of the two rotor units, which perfectly followed the predicted model for their rotational behavior. This detailed study on elucidating key parameters for control of rotary motion of third-generation molecular motors is essential for the design of more-advanced molecular machines based on light-driven rotary motion.

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