Thermal Conductivity Modeling of Nanofluids Contain MgO Particles by Employing Different Approaches

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Received: 26 December 2019; Accepted: 16 January 2020; Published: 1 February 2020

Abstract: The existence of solid-phase nanoparticles remarkably improves the thermal conductivity of the fluids. The enhancement in this property of the nanofluids is affected by different items such as the solid-phase volume fraction and dimensions, temperature, etc. In the current paper, three different mathematical models, including polynomial correlation, Multivariate Adaptive Regression Spline (MARS), and Group Method of Data Handling (GMDH), are applied to forecast the thermal conductivity of nanofluids containing MgO particles. The inputs of the model are the base fluid thermal conductivity, volume concentration, and average dimension of solid-phase, and nanofluids’ temperature. Comparing the proposed models revealed higher confidence of GMDH in estimating the thermal conductivity, which is attributed to its complicated structure and more appropriate consideration of the input’s interaction. The values of R-squared for the correlation, MARS, and GMDH are 0.9949, 0.9952, and 0.9991, respectively. In addition, based on the sensitivity analysis, the effect of thermal conductivity of the base fluid on the overall thermal conductivity of nanofluids is more remarkable compared with the other inputs such as volume fraction, temperature, and dimensions of the particles which are used as the inputs of the models.

Keywords: nanofluid; thermal conductivity; MgO nanoparticles; GMDH; MARS

1. Introduction

Thermal Conductivity (TC) of fluids influence their performance as heat transfer fluid in thermal mediums [1–3]. Adding nanodimensional solid structures into the pure conventional heat transfer fluids such as water, Ethylene Glycol (EG), and oils can remarkably enhance their TC [4–8]. For instance, Shameil et al. [9] found that the TC of DWCNT/ethylene glycol in 0.6% volume fraction of solid phase and 52 °C is enhanced by 24.9% compared with the pure base fluid. Guo et al. [10] measured TC of SiO2/water and SiO2/EG and observed that in 1% vol concentration, the TC of water- and EG-based nanofluids increased by 3.4% and 9.6%, respectively. In another experimental research study [11],...
the effect on $Al_2O_3$ nanoparticle dispersion in water and EG at different temperatures on the TC was investigated, and an increase in TC was observed in the case of solid particle dispersion in EG. Based on the literature review, an increment in the TC was dependent on the type of the base fluid, concentration, and temperature [12–15]. For instance, at 10 °C, the highest increases in the TC of water- and EG-based nanofluids were 13% and 20%, while these values increased to 15% and 25% at 70 °C, respectively. A higher increment in increased temperatures can be due to the Brownian motions of the solid particles [16]. In addition to the single type particles, hybrid nanostructures have been used in pure fluids for TC improvement. According to a study conducted by Hemmat Esfe et al. [17], adding $SiO_2 – DWCNT$ in 1.71%, volumetric concentration into EG resulted in up to a 38% increment in the TC.

Improved thermophysical feature of the fluids containing nanostructures makes them as favorable candidates for heat transfer fluid in thermal systems such as heat pipes, solar collectors, heat exchangers, etc. [18–24]. Elsayed et al. [25], carried out a numerical study on heat transfer of turbulent flow inside a helically coiled tube and concluded that using $Al_2O_3$/water instead of water led to 60% increase in heat transfer coefficient. MgO is one of the most attractive materials for preparing nanofluids due to its ability in providing more appropriate thermal features compared with other metal oxide particles [26,27]. Nanofluids containing MgO particles are widely utilized in different systems in order to achieve improved efficiency and heat transfer. Verma et al. [28] used MgO/water in a flat plate solar collector and observed that employing the nanofluid in 0.75% vol concentration instead of water resulted in up to 9.34% and 32.23% increases in the thermal and energetic efficiencies, respectively. Menlik et al. [29] applied MgO/water nanofluid in a heat pipe and observed that employing the nanofluid led to a 26% enhancement in the effectiveness of nanofluid-charged heat pipe.

Several methods and approaches are suggested for estimating the thermophysical properties of the nanofluids [30–33]. Artificial Neural Networks (ANNs), Support Vector Machines (SVMs), and correlation obtained by curve fitting are among the most applicable ones used in recent years [34–37]. Wu et al. [38] utilized curve fitting for the TC modeling of ZnO-multi walled carbon nano tube (MWCNT)/engine oil nanofluid by using the solid phase fraction and temperature as the inputs and observed that the proposed correlation was able to predict the TC of the nanofluid with maximum deviation lower than 1%. In another research, Hemmat et al. [39] proposed a correlation-based model on similar inputs for forecasting the TC of CuO/EG-water nanofluid. The value of R-squared for their proposed correlation was 0.9850. In the majority of the proposed models for TC forecasting [39], just temperature and volume fraction are considered for modeling, while adding the dimensions of the solid-phase result in finding more comprehensive models with applicability for different case studies [40,41]; in this regard, Ahmadi et al. [42] applied different artificial neural network (ANN)-based methods such as multilayer perceptron, Adaptive Neuro-Fuzzy Inference System (ANFIS) and Radial Basis Function (RBF) for modeling the TC of TiO$_2$/water nanofluid. The closeness of the estimated values by the models and the experimental values demonstrated the confident performance of ANNs for modeling.

The present paper is focused on the TC modeling of the nanofluids containing MgO particles for different values of temperature, size, volume fraction, and base fluids’ TC. In this regard, different approaches such as polynomial correlation, multivariate adaptive regression spline (MARS), and group method of data handling (GMDH) ANN are employed. Finally, the outputs of the models are compared with the actual values of nanofluids’ TC, obtained in different experimental studies, to evaluate the confidence of the models based on different statistical criteria. Moreover, the relative importance of the inputs is determined and explained.

2. Methodology

In the present article, three methods are employed for estimating the TC of nanofluids containing MgO particles. In the first stage, a polynomial of degree two is used for the regression. The main advantages of using polynomials for proposing predictive models are their ease for utilization and simplicity of the structure. Afterward, MARS and GMDH ANN are employed for forecasting the TC.
of the nanofluids. MARS approach is a nonparametric type of regression method which utilizes some basis functions for modeling complex input-output relationships. This model can be expressed as:

\[ y = f(X) + e \]  

(1)

where \( X \) refers to independent input variables, \( y \) is the output, \( f \) is the weighted basis function which is dependent on the inputs, and \( e \) denotes the error vector. In the MARS technique, piecewise linear regression functions are used in order to fit data and find nonlinear relationships between the inputs and the output. The relationships are found by employing piecewise polynomials and sets of coefficients [43]. This model is achieved by fitting the basis functions into distinct ranges of input variables. Put et al. [44] investigated the MARS global technique. It is defined as follows (Equation (2)):

\[ \hat{y} = \beta_0 + \sum_{m=1}^{M} \beta_m h_m(X) \]  

(2)

\( \hat{y} \) and \( \beta_0 \) in Equation (2) are the prognosticated response and the coefficient of the basis function, respectively. The \( m \)th basic function is represented as \( h_m(X) \). It can have the form of either a single polynomial or a combination of more polynomial functions. Furthermore, \( \beta_m \) is a coefficient relating to the \( m \)th basis function. The number of basis functions that the MARS algorithm takes into consideration is counted by \( M \).

In the MARS technique, there are three main stages. The first one is known as the constructive step. It adds the basis functions using a stepwise forward method. In addition, two substantial parameters (i.e., locations of nodes and the predictor) are being selected in this stage of the MARS technique. They have considerable effect on the accuracy of the results.

In the first step, interactions are given in order to study their relevance with the model fit refinement. Secondly, with the aim of enhancing the prediction, the goal is to eliminate the superfluous basis functions. This is done through a backward stepwise approach. In the MARS technique, the Generalized Cross-Validation (GCV) is used as a criterion in order to specify the most effective model among many currently available models. A high value of GCV makes a smaller model, and a lower quantity for GCV suggests a bigger produced model. Equation (5) shows the GCV criterion [43,45]:

\[ GCV = \frac{1}{N} \sum_{i=1}^{N} \frac{(y_i - f(X_i))^2}{[1 - \frac{\tilde{C}(M)}{N}]^2} \]  

(3)

The term \( [1 - \frac{\tilde{C}(M)}{N}]^2 \) in Equation (3) is a complexity function. Furthermore, \( \tilde{C}(M) \) is defined as \( C(M) + dM \). Here, \( d \) is the cost of each of the basis functions. It can be decided based on the user’s requirements. This parameter specifies the soothing of the approach. \( C(M) \) is considered as the value of the elements that should be fit. The parameter \( d \) in Equation (3) sets the number of the basis functions that can be eliminated.

It can be inferred that as the cost increases, more basis functions are eradicated. Ultimately, in the third stage, the optimized MARS technique is determined. This is done based on the assessment of the characteristics of the proposed fit models. More details about this method can be found in Refs [43,45]. GCV function is utilized in order to figure out the significance score of the input variables. The input variables’ relative importance indicates an increment in the quantity of the GCV as the applied basis function having specific variables are dropped and the other basis functions refit to the target, in the genuine form, by applying ordinary least square (OLS) regression. The details of this approach are represented in [43,46].

ANNs are applicable in different fields of study for predicting the behavior of the systems and their modeling [47–51]. The third approach used for forecasting the TC of the nanofluids with MgO
particles is GMDH. This approach has some advantages in comparison with other conventional ANNs, such as no requirement for precondition definitions, including the number of layers and neurons, due to its self-regulating property. In this approach, the repetitive procedure is performed in order to accurate calculation of the variable considered as the target \( P \). The schematic of the procedure applied in GMDH is shown in Figure 1. In the process of modeling by applying GMDH, polynomials of degree two are utilized in the first step and its complicity increases by an increment in the number of layers. An increase in the number of layers depends on the required effectiveness of the model. In this procedure, in the case of having \( n \) inputs and an output, Kolmogorov–Gabor polynomial is generated to form the network.

\[
P = a_0 + \sum_{i=1}^{n} a_1X_i + \sum_{i=1}^{n} \sum_{j=1}^{n} a_{ij}X_iX_j + \sum_{i=1}^{n} \sum_{j=1}^{n} \sum_{k=1}^{n} a_{ijk}X_iX_jX_k + \cdots
\]

In this equation, \( X \) refers to the vector used as input, \( \omega \) is the weight vector, and \( P \) is the forecasted output. The output of the model is determined by utilizing the least square approach by determining the minimum mean square error value. In the case of using \( Xi \) and \( Xj \) as the inputs, the overall obtained polynomial can be defined as:

\[
P = a_0 + a_1X_i + a_2X_j + a_3X_iX_j + a_4X_i^2 + a_5X_j^2
\]

This approach is explained with more details in several references [53–55].

3. Results and Discussion

Since the aim of the present study is proposing a model with applicability for different base fluids in various temperature, volume fraction, and dimensions of particles, several references were used for data extraction [27,56–60]. The base fluids of the considered case studies were engine oil, water, EG, and mixtures of EG-water. In order to quantitatively consider the impact of the base fluid in the model, their TC at 25 °C was added to the volume fraction, size, and temperature, which have been used in previous studies. The ranges of temperature and volume fraction of the extracted data were 10–55 °C and 0.1–7.2%, respectively. Nanoparticles with average diameters in the range of 10 and 60 mm were used in the case studies.
As was previously noted, a polynomial of degree two is used for the modeling. The structure of the polynomial is designed as:

\[ TC = a \cdot x_1 + b \cdot x_2 + c \cdot x_3 + d \cdot x_4 + e \cdot x_1^2 + f \cdot x_2^2 + g \cdot x_3^2 + h \cdot x_4^2 + i \cdot x_1 \cdot x_2 + j \cdot x_1 \cdot x_3 + k \cdot x_1 \cdot x_4 + l \cdot x_2 \cdot x_3 + m \cdot x_2 \cdot x_4 + n \cdot x_3 \cdot x_4 + o \]  

where \( x_1, x_2, x_3, \) and \( x_4 \) are the TC of the base fluid, size of the particles, volume fraction, and temperature, respectively. The obtained values of the abovementioned correlation are represented in Table 1.

Table 1. Determined coefficients of the polynomial.

|   | 0.960011 | 0.002045 | 0.006512 | −0.00081 | −0.20459 | −0.000024 | 0.000235 | −0.00001 |
|---|---------|---------|---------|---------|---------|---------|---------|---------|
| a | b       | c       | d       | e       | f       | g       | h       | i       |
| j | k       | l       | m       | n       | o       |         |         |         |
| −0.00076 | 0.051041 | 0.007562 | −0.00014 | 0       | 0.00006 | −0.01792 |         |         |

In Figure 2, the obtained values of the TC are compared with the actual quantities measured in the experimental researches. In this case, the R-squared value is 0.9949. In addition to R-squared, the relative deviation of the model is determined to indicate the confidence of the model. The corresponding relative deviation for each data index is shown in Figure 3. In this case, the maximum relative deviation is about 12.2%.

![Figure 2](image.png)

**Figure 2.** Comparison between the values obtained by the correlation and experimental data.

In the second step, the MARS method is used for modeling the TC of the nanofluids. The determined relationships between the inputs and the TC by employing the MARS approach is as below:

\[ TC = 0.278929 + 1.24943 \cdot BF1 + 0.955071 \cdot BF2 + 0.0210546 \cdot BF3 - 0.0804188 \cdot BF4 - 0.441445 \cdot BF5 - 0.00479538 \cdot BF7 - 0.00058189 \cdot BF8 - 0.000408513 \cdot BF9 - 0.00911003 \cdot BF10 + 0.00230784 \cdot BF12 \]  

(7)
The basis functions used in the abovementioned equations are shown in Table 2.

| Basis Functions | BF1                  | BF2                  | BF3                  | BF4                  | BF5                  |
|-----------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| Relationship    | \( \max(0, x_1 - 0.251) \) | \( \max(0, 0.251 - x_1) \) | \( \max(0, x_3 - 0.25) \) | \( \max(0, 0.25 - x_3) \) | \( \max(0, x_1 - 0.408) \) |
| Basis Functions | BF7                  | BF8                  | BF9                  | BF10                 | BF12                 |
| Relationship    | \( \max(0, x_4 - 50) \) | \( \max(0, 50 - x_4) \) | \( \max(0, x_2 - 10) \) | \( \max(0, x_4 - 4) \) | \( \max(0, x_4 - 45) \) |

In Figure 4, the forecasted values of TC are compared with the corresponded quantities measured in the experimental researches. In this case, the R-squared is equal to 0.9952. The higher value of the R-squared in the case of using the MARS method compared with the proposed correlation reveals the higher confidence of the model. The improved accuracy of the model by employing the MARS approach can be attributed to its more complex structure, which results in better consideration of input variables interactions. In addition to R-squared, these methods can be compared on the basis of relative deviation. As shown in Figure 5, the maximum value of relative deviation in the case of applying MARS for TC modeling is 13.76%; however, in most cases, its values are lower compared with the proposed correlation.

Finally, a model is proposed for the TC of the nanofluids by using GMDH ANN. The obtained relationship for the inputs and the output of the model is:

\[
TC = -8.7104 \times 10^{-5} + N153 \times 0.0556369 + N2 \times 0.944621
\]  

(8)

The procedure of determining the coefficients are represented in Appendix A. In this case, the R-squared is 0.9991, which is higher compared with the determined values of the previous models. In Figure 6, the TCs obtained with the model and actual values are compared. In addition, comparing the values of relative deviation demonstrates more confidence in the prediction in the case of using GMDH in comparison with using the MARS method and mathematical correlation. As illustrated in Figure 7, the maximum absolute value of the relative deviation is approximately 3.18% when GMDH was applied for modeling.
R-squared is 0.9991, which is higher compared with the determined values of the previous models. Figure 7, the maximum absolute value of the relative deviation is approximately 3.18% when GMDH is compared with the MARS method and mathematical correlation. As illustrated in Figure 6, the TCs obtained with the model and actual values are compared. In addition, comparing the values of relative deviation demonstrates more confidence in the prediction in the case of using GMDH in comparison with using the MARS method and mathematical correlation. In Figure 9, the importance of variables is shown.

Finally, a model is proposed for the TC of the nanofluids by using GMDH ANN. The obtained relationship for the inputs and the output of the model is:

\[
\text{TC} = a_1 \cdot 2^{0.944621} + a_2 \cdot (0.0556369 \cdot T + 153) \cdot (0.0843939 \cdot \nu + 119) \cdot \rho \cdot (1 - 0.251) \cdot \varepsilon - 0.251
\]

In order to have a deeper insight into the accuracy of the models in predicting the data, using the average absolute relative deviation can be more useful, which provides the possibility of comparing the accuracy of the models for the total data. As shown in Figure 8, the average absolute relative deviation of the correlation, MARS, and GMDH in modeling, are approximately 3.22%, 2.03%, and 0.90%, respectively.

Deviation in the case of applying MARS for TC modeling is 13.76%; however, in most cases, its values are lower compared with the proposed correlation.

The relative importance of the inputs provides useful information about the role of each input on the outputs of the model. Based on the sensitivity analysis, the TC of the base fluid has the most crucial role in the value of the nanofluids' TC.

**Figure 4.** Comparison between the values obtained by the MARS method and the experimental data.

**Figure 5.** Relative deviation vs. data index for the MARS model.

**Figure 6.** Comparison between the values obtained by the GMDH method and the experimental data.
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The relative importance of the inputs provides useful information about the role of each input on the outputs of the model. Based on the sensitivity analysis, the TC of the base fluid has the most crucial role in the value of the nanofluids’ TC. In Figure 9, the importance of variables is shown.
4. Conclusions

In this paper, three methods, including a mathematical correlation, MARS, and GMDH ANN were applied to forecast the thermal conductivity of nanofluids containing MgO nanoparticles. The inputs of the proposed models were thermal conductivity of the base fluid, volume fraction, and dimensions of CuO particles and temperature. Models comparison revealed that employing GMDH resulted in the highest confidence. The average absolute relative deviations of the models in the cases of employing correlation, MARS, and GMDH methods were approximately 3.22%, 2.03%, and 0.90%, respectively. In addition, based on the performed sensitivity analysis, thermal conductivity of the base fluid had the most noticeable impact on the thermal conductivity of the nanofluids. The R-squared of the proposed models by using the correlation, MARS and GMDH approaches, were 0.9949, 0.9952, and 0.9991, respectively. According to these determined values, all of the models are reliable and appropriate for forecasting the thermal conductivity of the nanofluids with dispersed MgO particles.

Author Contributions: The N.W. and M.A.N. conducted modeling and writing, revising the article is carried out by the M.S.S. A.M. and I.T. supervised the research and edited it. All authors have read and agreed to the published version of the manuscript.

Funding: This research received no external funding.

Conflicts of Interest: The authors declare no conflicts of interest.

Appendix A

\[
TC = -8.7104 \times 10^{-5} + N153 \times 0.0556369 + N2 \times 0.944621 \\
N2 = 6.33392 \times 10^{-5} - N73 \times 0.111613 + N3 \times 1.11143 \\
N3 = 0.00138188 + N59 \times N5 \times 74.1406 - N59^2 \times 37.0879 + N5 \times 0.995333 - N5^2 \times 37.0464 \\
N5 = -0.00147952 + N31 \times 0.241927 - N31 \times N6 \times 73.7483 + N31^2 \times 36.7664 + N6 \times 0.763533 + N6^2 \times 36.9748 \\
N6 = 0.0002285 - N114 \times 0.460449 + N14 \times 1.45977
\]
\[ N_{14} = 0.000105035 + N_{18} \cdot 0.643206 + N_{18} \cdot N_{25} \cdot 28.8074 - N_{18}^2 \cdot 14.4924 + N_{25} \cdot 0.357674 - N_{25}^2 \cdot 14.3163 \]

\[ N_{25} = 0.00218015 + N_{332} \cdot N_{54} \cdot 3.67579 - N_{332}^2 \cdot 2.02706 + N_{54} \cdot 0.997428 - N_{54}^2 \cdot 1.65177 \]

\[ N_{54} = -0.0408802 - N_{355} \cdot N_{74} \cdot 0.693239 + N_{355}^2 \cdot 0.46511 + N_{74} \cdot 1.17673 + N_{74}^2 \cdot 0.0616494 \]

\[ N_{355} = 0.371309 + N_{360} \cdot 0.71474 - N_{364} \cdot 1.58917 + N_{364}^2 \cdot 2.24705 \]

\[ N_{364} = 3.27276 + x_4 \cdot 0.0100847 - x_4^2 \cdot 0.000152815 - N_{370} \cdot 17.6064 + N_{370}^2 \cdot 24.9277 \]

\[ N_{332} = -0.370344 + N_{342} \cdot 0.804179 + N_{342} \cdot N_{368} \cdot 1.20998 - N_{342}^2 \cdot 0.315614 + N_{368} \cdot 2.05621 - N_{368}^2 \cdot 3.08519 \]

\[ N_{368} = 2.7631 - N_{371} \cdot 15.8134 + N_{371}^2 \cdot 25.3292 \]

\[ N_{342} = -0.00477946 + x_2 \cdot 0.000167309 - x_2 \cdot N_{343} \cdot 0.000270589 - x_2^2 \cdot 9.30425 \cdot 10^{-7} + N_{343} \cdot 1.00992 \]

\[ N_{18} = -0.00710574 - N_{196} \cdot 1.02626 - N_{196} \cdot N_{41} \cdot 1.99319 + N_{196}^2 \cdot 1.94146 + N_{41} \cdot 2.06698 \]

\[ N_{41} = 0.00157139 + N_{304} \cdot N_{69} \cdot 5.7359 - N_{304}^2 \cdot 3.01962 + N_{69} \cdot 1.00069 - N_{69}^2 \cdot 2.71984 \]

\[ N_{69} = 0.00476153 + N_{137} \cdot 0.994991 + N_{137} \cdot N_{187} \cdot 0.832487 - N_{137}^2 \cdot 0.822307 \]

\[ N_{137} = 0.00611404 + x_1 \cdot 1.06531 - x_1 \cdot N_{175} \cdot 3.09998 + N_{175}^2 \cdot 2.85239 \]

\[ N_{175} = 0.0749914 - x_4 \cdot 0.00157427 + x_4 \cdot N_{227} \cdot 0.00678305 + N_{227} \cdot 0.598162 + N_{227}^2 \cdot 0.279983 \]

\[ N_{304} = -0.386619 + N_{337} \cdot 0.721253 + N_{337} \cdot N_{358} \cdot 1.48285 - N_{337}^2 \cdot 0.277372 + N_{358} \cdot 2.17904 - N_{358}^2 \cdot 3.35703 \]

\[ N_{358} = 2.16103 - N_{370} \cdot 11.3861 - N_{370} \cdot N_{371} \cdot 17.9324 + N_{370}^2 \cdot 25.0097 + N_{371}^2 \cdot 10.3783 \]
\[ N_{337} = 0.0210866 - x_2 \cdot 0.000486486 + x_2^2 \cdot 3.01016 \cdot 10^{-7} + N_{348} \cdot 0.993111 \]

\[ N_{196} = 0.0776005 - x_4 \cdot 0.00165255 + x_4 \cdot N_{243} \cdot 0.00696503 + N_{243} \cdot 0.591801 + N_{243}^2 \cdot 0.28152 \]

\[ N_{243} = 0.23064 + N_{249} \cdot 0.98187 + N_{249}^2 \cdot 0.0104777 - N_{369} \cdot 1.37367 + N_{369}^2 \cdot 2.06441 \]

\[ N_{114} = 0.0141143 + x_1 \cdot 0.584343 - x_1 \cdot N_{144} \cdot 1.99686 + N_{144} \cdot 0.380788 + N_{144}^2 \cdot 1.91876 \]

\[ N_{144} = -0.00204878 + N_{167} \cdot 0.382578 + N_{167} \cdot N_{202} \cdot 0.647188 + N_{202} \cdot 0.626817 - N_{202}^2 \cdot 0.655717 \]

\[ N_{202} = -0.044274 - N_{249} \cdot 27.4437 - N_{249} \cdot N_{247} \cdot 80.0187 + N_{249}^2 \cdot 80.0501 + N_{247} \cdot 28.5628 \]

\[ N_{247} = 0.00621484 + N_{249} \cdot 0.963485 + N_{348}^2 \cdot 0.0481015 \]

\[ N_{31} = 0.00441769 + N_{226} \cdot 0.364219 - N_{226} \cdot N_{32} \cdot 12.9012 + N_{226}^2 \cdot 6.05236 + N_{32} \cdot 0.610084 + N_{32}^2 \cdot 6.87458 \]

\[ N_{52} = -0.0646652 + N_{363} \cdot 0.201776 - N_{363} \cdot N_{74} \cdot 0.270059 + N_{74} \cdot 1.08277 \]

\[ N_{74} = -0.000760788 + N_{132} \cdot 1.00215 - N_{132}^2 \cdot 0.40679 + N_{187}^2 \cdot 0.407217 \]

\[ N_{187} = 0.00418857 - N_{207} \cdot 0.516945 - N_{207} \cdot N_{240} \cdot 125.356 + N_{207}^2 \cdot 65.7687 + N_{240} \cdot 1.48596 + N_{240}^2 \cdot 59.6245 \]

\[ N_{240} = 0.0125984 + N_{245} \cdot 1.84031 + N_{245} \cdot N_{300} \cdot 2.21798 - N_{245}^2 \cdot 2.14763 - N_{300} \cdot 0.901969 \]

\[ N_{300} = -0.162121 + N_{343} \cdot 0.838859 + N_{343} \cdot N_{371} \cdot 0.94242 - N_{343}^2 \cdot 0.227397 + N_{371} \cdot 0.624239 - N_{371}^2 \cdot 0.638309 \]

\[ N_{226} = 0.0234405 + N_{245} \cdot 2.88634 + N_{245} \cdot N_{289} \cdot 5.00976 - N_{245}^2 \cdot 4.87702 - N_{289} \cdot 2.00173 \]

\[ N_{289} = -0.145798 + N_{348} \cdot 0.925865 + N_{348} \cdot N_{371} \cdot 0.674947 - N_{348}^2 \cdot 0.222066 + N_{371} \cdot 0.360132 \]
\[ N_{59} = 0.00762732 + N_{204} \cdot 0.956563 - N_{204} \cdot N_{77} \cdot 8.63878 + N_{204}^2 \cdot 3.34262 + N_{77}^2 \cdot 5.34632 \]

\[ N_{77} = -0.0184702 + N_{139} \cdot 1.08486 - N_{139} \cdot N_{349} \cdot 0.895069 + N_{139}^2 \cdot 0.312548 + N_{349}^2 \cdot 0.472899 \]

\[ N_{349} = -0.24874 + N_{350}^2 \cdot 1.28051 + N_{354} \cdot 2.17015 - N_{354}^2 \cdot 2.53189 \]

\[ N_{354} = 0.542463 + N_{360} \cdot 2.65141 + N_{360} \cdot N_{365} \cdot 11.6912 - N_{360}^2 \cdot 8.42761 - N_{365} \cdot 4.35281 \]

\[ N_{365} = 1.33214 + x_2 \cdot 0.0149331 - x_2 \cdot N_{370} \cdot 0.0333006 - x_2^2 \cdot 4.34831 \cdot 10^{-5} - N_{370} \cdot 7.62649 + N_{370}^2 \cdot 13.0534 \]

\[ N_{370} = 0.768367 + x_4 \cdot 0.0249707 - x_4 \cdot N_{369} \cdot 0.0607055 - x_4^2 \cdot 7.14588 \cdot 10^{-5} - N_{369} \cdot 6.01 + N_{369}^2 \cdot 13.3676 \]

\[ N_{366} = 2.54124 - x_2 \cdot N_{371} \cdot 0.0147577 + x_2^2 \cdot 5.02424 \cdot 10^{-5} - N_{371} \cdot 14.3422 + N_{371}^2 \cdot 23.8769 \]

\[ N_{371} = 0.315366 + x_3 \cdot 0.0469567 - x_3^2 \cdot 0.00657724 - x_4^2 \cdot 1.9964 \cdot 10^{-5} \]

\[ N_{363} = 3.3063 - N_{369} \cdot 9.4594 + N_{369} \cdot N_{370} \cdot 16.3706 + N_{369}^2 \cdot 6.88907 - N_{370} \cdot 8.43063 + N_{370}^2 \cdot 3.48156 \]

\[ N_{370} = 0.559466 - x_2 \cdot 0.00928795 + x_2 \cdot x_4 \cdot 7.29825 \cdot 10^{-5} + x_2^2 \cdot 6.86844 \cdot 10^{-5} - x_4^2 \cdot 5.50523 \cdot 10^{-5} \]

\[ N_{139} = 0.0599519 - x_4 \cdot 0.000668139 + x_4 \cdot N_{198} \cdot 0.00599168 - x_4^2 \cdot 8.77286 \cdot 10^{-6} + N_{198} \cdot 0.604476 + N_{198}^2 \cdot 0.298508 \]

\[ N_{198} = -0.00739919 + x_1 \cdot 1.15248 - x_1 \cdot N_{227} \cdot 3.26148 + N_{227}^2 \cdot 2.90253 \]

\[ N_{73} = -0.000752215 + N_{132} \cdot 1.00207 - N_{132} \cdot N_{188} \cdot 0.80864 + N_{188}^2 \cdot 0.808737 \]

\[ N_{188} = 0.00842781 - N_{207} \cdot N_{239} \cdot 214.111 + N_{207}^2 \cdot 109.179 + N_{239} \cdot 0.946987 + N_{239}^2 \cdot 104.983 \]
\[ N239 = -0.0283368 + N245 \times 1.11063 - N245 \times N357 \times 0.350962 + N357^2 \times 0.273286 \]

\[ N357 = 5.46278 - x_2 \times 0.0177107 + x_2 \times N369 \times 0.0722021 - x_2^2 \times 6.09357 \times 10^{-5} - N369 \times 30.525 + N369^2 \times 43.7799 \]

\[ N245 = 0.00469092 + N249 \times 0.986125 + N249 \times N343 \times 7.24005 - N249^2 \times 3.63278 - N343^2 \times 3.58576 \]

\[ N207 = 0.0117824 + N219 \times 1.38854 + N219 \times N339 \times 9.20926 - N219^2 \times 5.16005 - N339 \times 0.440334 - N339^2 \times 3.97121 \]

\[ N339 = -0.0136465 + x_4 \times 0.000312714 + N343 \times 1.00594 \]

\[ N219 = 0.000436997 + x_1 \times 1.09273 - x_1 \times N249 \times 3.18854 + N249^2 \times 2.91325 \]

\[ N132 = 0.0101058 + x_1 \times 0.935141 - x_1 \times N167 \times 5.3548 + x_1^2 \times 1.51369 + N167 \times 0.092853 + N167^2 \times 3.68007 \]

\[ N167 = -0.0234471 + x_2 \times 0.00133983 - x_2 \times N201 \times 0.000893987 - x_2^2 \times 1.84993 \times 10^{-5} + N201 \times 1.05634 - N201^2 \times 0.0308196 \]

\[ N153 = 0.00644219 + N183 \times 0.467566 - N183 \times N204 \times 36.2981 + N183^2 \times 18.1295 + N204 \times 0.49205 + N204^2 \times 18.2057 \]

\[ N204 = -0.0027637 + N227 \times 1.56905 + N227 \times N298 \times 29.99 - N227^2 \times 15.4078 - N298 \times 0.517987 - N298^2 \times 14.6533 \]

\[ N298 = -0.213135 + x_1 \times 1.5415 - x_1^2 \times 0.716435 + N369 \times 0.529644 \]

\[ N369 = 0.424808 - x_2 \times 0.00602004 + x_2 \times x_3 \times 0.31487 \times 10^{-5} + x_2^2 \times 5.75127 \times 10^{-5} + x_3 \times 0.0422081 - x_3^2 \times 0.0066477 \]

\[ N227 = -0.00118403 + x_3 \times 0.0168248 + N343 \times 0.794964 + N343^2 \times 0.266735 \]

\[ N343 = -0.0165124 + x_1 \times 1.5302 - x_1^2 \times 0.674759 - x_2 \times 0.000460021 \]

\[ N183 = 0.000386682 - N201 \times 0.644518 - N201 \times N222 \times 109.562 + N201^2 \times 56.6588 + N222 \times 1.62812 + N222^2 \times 52.925 \]
\[ N_{222} = -0.00215233 + x_3 \cdot 0.0172009 + N_{348} \cdot 0.794615 + N_{348}^2 \cdot 0.268923 \]

\[ N_{348} = -0.0241623 + x_1 \cdot 1.39918 + x_1 \cdot x_4 \cdot 0.00120499 - x_1^2 \cdot 0.521387 \]

\[ N_{201} = 0.0833688 - x_4 \cdot 0.00161256 + x_4 \cdot N_{249} \cdot 0.00682585 + N_{249} \cdot 0.555885 + N_{249}^2 \cdot 0.332771 \]

\[ N_{249} = -0.0483794 + x_1 \cdot 1.37161 - x_1^2 \cdot 0.430654 \]

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