VVV SURVEY OBSERVATIONS OF A MICROLENSING STELLAR MASS BLACK HOLE CANDIDATE IN THE FIELD OF THE GLOBULAR CLUSTER NGC 6553

D. Minniti1,2,3, R. Contreras Ramos2,4, J. Alonso-García5,2, T. Anguita1,2, M. Catelan2,4, F. Gran2,4, V. Motta6, G. Muro7, K. Rojas6, and R. K. Saito8

1 Departamento de Ciencias Físicas, Universidad Andres Bello, Campus La Casona, Fernández Concha 700, Santiago, Chile; dante@astrofisica.cl
2 Millennium Institute of Astrophysics, Av. Víncula Mackenna 4860, 782-0436 Macul, Santiago, Chile
3 Vatican Observatory, Vatican City State, I-00120, Italy
4 Instituto de Astrofísica, Pontificia Universidad Católica de Chile, Av. Víncula Mackenna 4860, 782-0436 Macul, Chile
5 Universidad de Astronomía, Facultad Cs. Básicas, Universidad de Antofagasta, Avda. U. de Antofagasta 02000, Antofagasta, Chile
6 Instituto de Física y Astronomía, Facultad de Ciencias, Universidad de Valparaíso, Av. Gran Bretaña 1111, Playa Ancha, Valparaíso, Chile
7 Institut voor Sterrenkunde, K.U. Leuven, Celestijnenlaan 200B, B-1 Herlee, Belgium
8 Universidade Federal de Sergipe, Departamento de Física, Aracajú, SE, Brazil

Received 2015 April 17; accepted 2015 August 3; published 2015 September 3

ABSTRACT

We report the discovery of a large timescale candidate microlensing event of a bulge stellar source based on near-infrared observations with the VISTA Variables in the Vía Láctea (VVV) survey. The new microlensing event is projected only 3.5 arcmin away from the center of the globular cluster NGC 6553. The source appears to be a bulge giant star with magnitude $K_s = 13.52$, based on the position in the color–magnitude diagram. The foreground lens may be located in the globular cluster, which has well-known parameters such as distance and proper motions. If the lens is a cluster member, we can directly estimate its mass simply following Paczynski which is a modified version of the more general case due to Refsdal. In that case, the lens would be a massive stellar remnant, with $M = 1.5–3.5 M_\odot$. If the blending fraction of the microlensing event appears to be small, and this lens would represent a good isolated black hole (BH) candidate, that would be the oldest BH known. Alternative explanations (with a larger blending fraction) also point to a massive stellar remnant if the lens is located in the Galactic disk and does not belong to the globular cluster.

Key words: globular clusters: individual (NGC 6553) – gravitational lensing: micro – infrared: stars – surveys

Supporting material: machine-readable table

1. INTRODUCTION

Microlensing is the best (and so far the only) tool to detect isolated stellar mass black holes (BHs; see Mao 2012). The microlensing projects have discovered a few candidate stellar-mass BH lenses toward the Galactic bulge (Agol et al. 2002; Bennett et al. 2002; Poindexter et al. 2005; Mao 2012). Gould & Salim (1999) specifically applied astrometric microlensing in order to measure the masses of BHs. Although the measurements remain challenging, this method is important for future measurements from space (Gould & Yee 2014).

Refsdal (1964) showed that the mass $M$ of a gravitational lens is related to observables ($\mu_{rel}$, $\pi_{rel}$, $t_E$) by

$$M = \frac{\theta_E^2}{\kappa \pi_{rel}}, \quad \theta_E = \mu_{rel} t_E, \quad \kappa = \frac{4G}{c^2} \approx 8.1 \text{ mas} \frac{M_\odot}{M}$$

where $t_E$ is the Einstein crossing time derived from the event light curve and $\pi_{rel}$ and $\mu_{rel}$ are the lens-source relative parallax and proper motion respectively. While Refsdal (1964) clearly had in mind that the lens and source could both be seen, Paczynski (1994) pointed out that for globular-cluster lenses detected via their magnification of Galactic-bar sources, $\pi_{rel}$ and $\mu_{rel}$ can potentially be estimated without directly observing the lens. This opens the possibility that the method could be applied to BH lenses. The main advantage of such a search is that the microlensing geometry is more certain, and there is a direct relationship between the lens mass and the time scale of the event. This technique was successful in the case of the first confirmed globular cluster microlensing event in M22 (NGC6656) due to a low-mass star (Pietrukowicz et al. 2005, 2012). Later, another microlensing event in close projection to the globular cluster NGC 6553 was reported (Yee et al. 2013), which also turned out to be a low-mass lens, possibly with a planet. However, the suggestion by Paczynski (1994, 1996) seems to be a promising way to search and measure heavy remnants (neutron stars, NSs, or BHs) in spite of the technical challenges.

Here we report the discovery of a long-timescale candidate microlensing event of a bulge stellar source projected only 3.5 arcmin away from the center of the globular cluster NGC 6553. If lens membership to the cluster is confirmed, the lens could be a massive stellar remnant, possibly a BH with $M = 2 M_\odot$. Section 2 presents the VVV Survey observations of the microlensing event. Section 3 discusses the globular cluster NGC 6553 where the lens may reside. Section 4 shows the measured parameters of the lens, and Section 5 summarizes the conclusions and future tests.

2. VVV SURVEY OBSERVATIONS OF THE MICROLENSING EVENT

VISTA Variables in the Vía Láctea (VVV) is a public ESO near-infrared (IR) variability survey aimed at scanning the inner Milky Way (Minniti et al. 2010). The observations are acquired with the VISTA 4 m telescope at ESO Paranal Observatory (Sutherland et al. 2015). The VVV survey covers an area of 562 sqdeg in the inner disk and bulge of the Milky Way. The VVV database now contains multicolor $(ZYJHK)$ photometry, and multiple epochs in the $K_s$-band, monitoring
about a billion sources in total (Saito et al. 2012). The $K_s$-band observations continue, and the variability light curves so far span from 2010 to 2015. This large database enables a number of studies of different variable objects, including microlensing events (Catelan et al. 2013; Hempel et al. 2014).

We have started to search for variable stars using the VVV Survey data in the fields of 36 globular clusters toward the Galactic bulge. The data reductions and photometry have been described in detail by Alonso-García et al. (2015), where our first results for the globular clusters 2MASS-GC02 and Terzan 10 are also presented. Briefly, the individual VVV Survey images are reduced, astrometrized and stacked by the Cambridge Astronomy Survey Unit (CASU) using the VISTA Data Flow System pipeline (Emerson et al. 2004; Hambly et al. 2004; Irwin et al. 2004), and the photometry is calibrated onto the VISTA filter system. Then we carry out point-spread function photometry on the individual processed stacked images using an updated version of DoPHOT (Schecter et al. 1993; Alonso-García et al. 2012). The photometry for each object in the different images available was cross-correlated using the STILTS package Taylor (2006), and the light curves generated were then analyzed for variability (see Alonso-García et al. 2015).

During this near-IR search for variable stars in the field of the globular cluster NGC 6553 (R. Contreras Ramos et al. 2015, in preparation), we discovered a candidate microlensing event located at R.A.(2000) = 18:09:13.86, decl.(2000) = $-25:57:52.7$, that is only 3.5 arcmin away from the cluster center. This event peaked in the 2012 bulge season (on 2012 July 8). The brightness of the object increased by about 0.7 mag in the $K_s$-band over 50 days, reaching a magnitude of $K_s = 12.8$, and then fading to a constant level of $K_s = 13.5$.

Table 1 shows the $K_s$-band observations for this object. The $K_s$-band epochs correspond to different nights, and the seeing for the majority of them was very good, between 0.6 and 1.2 arcsec.

| Epoch (MD) | $K_s$ | $\sigma_{K_s}$ |
|------------|------|---------------|
| 56363.376890 | 13.509 | 0.013 |
| 55298.333635 | 13.509 | 0.015 |
| 55491.015648 | 13.528 | 0.013 |
| 55778.139393 | 13.495 | 0.013 |
| 55804.103650 | 13.543 | 0.012 |

(This table is available in its entirety in machine-readable form.)

A microlensing event is particularly interesting. The bulge globular cluster NGC 6553 has been well studied, and its physical parameters are relatively well known. NGC 6553 is an old and metal-rich bulge globular cluster (Minniti 1995; Ortolani et al. 1995; Barbary et al. 1998; Zoccali et al. 2001; Alves-Brito et al. 2006). This cluster is moderately concentrated with a core radius $r_c = 0.55$ arcmin, and a tidal radius $r_t = 8.16$ arcmin. It is very reddened, with $E(B-V) = 0.73$, $A_V = 2.26$, and $A_K = 0.23$ (Barbuy et al. 1998). Particularly relevant for this work is the distance of the cluster. We adopt a distance of 6.0 kpc for this cluster following Alves-Brito et al. (2006), as listed in the 2010 version of Harris (1996) catalog, noting that the distance uncertainty adds to the total error budget. We observe the cluster horizontal branch (HB) at $K_s = 12.5$ (Figure 3), which is consistent with this distance measurement.

Zoccali et al. (2001) measured a relative proper motion of NGC 6553 with respect to the bulge of $\mu_\alpha = 5.89$ and $\mu_\delta = 0.42$ mas/yr. This gives a relative mean proper motion difference from an unresolved source. However, we have fitted a microlensing light curve, obtaining two equally good fits with $\chi^2 = 200$: an unblended and a blended fit, that are discussed in turn in the following sections. Both fits are very good, with the following microlensing parameters: Case A (without blending): baseline magnitude $K_{s,0} = 13.515 \pm 0.002$, impact parameter $u_0 = 0.62 \pm 0.004$, time of closest approach $t_0 = 56117.5 \pm 0.43$, Einstein timescale $t_\text{E} = 51.3 \pm 0.8$ days, blending $f = 1.00$, and $\chi^2 = 201$. Case B (with blending): baseline magnitude $K_{s,0} = 13.515 \pm 0.002$, impact parameter $u_0 = 0.46 \pm 0.08$, time of closest approach $t_0 = 56117.4 \pm 0.42$, Einstein timescale $t_\text{E} = 62.5 \pm 9$ days, blending $f = 0.61 \pm 0.17$, and $\chi^2 = 199$.

The values obtained for $\chi^2$ show that there is no improvement in the curve fitting when a blending factor is included. Also, the VVV Survey is designed to monitor variable stars, and the light curve is not frequently and evenly sampled, preventing us from using more complex models (with larger numbers of free parameters like those including the parallax effect) with better confidence than a simple microlensing light curve.

Can this be a variable star instead of a microlensing event? The main kinds of variable star contaminants are foreground dwarf novae and distant background SN, both of which are unlikely. The shape of the light curve is very symmetric, unlike the nova, dwarf novae or supernova light curves that typically show a fast rise and a slow decline. There are some exceptions, as some recurrent novae show symmetric outbursts (see for example, the light curve of GK Per9). However, we discard a dwarf nova outburst because of the light curve shape and also because our object is too red ($\Delta r = 1.0$) to be a dwarf nova. We also searched for variability in the region outside the peak but no signal of eclipses or ellipsoidal variations from a binary system were found as expected from a cataclysmic variable. Also, even though the VVV Survey data is deep enough to see background galaxies throughout the bulge, in this case no extended galaxy-like object that could be a supernova host galaxy is detected.

### 3. THE GLOBULAR CLUSTER NGC 6553

Because of its proximity to a globular cluster, this microlensing event is particularly interesting. The bulge globular cluster NGC 6553 has been well studied, and its physical parameters are relatively well known. NGC 6553 is an old and metal-rich bulge globular cluster (Minniti 1995; Ortolani et al. 1995; Barbary et al. 1998; Zoccali et al. 2001; Alves-Brito et al. 2006). This cluster is moderately concentrated with a core radius $r_c = 0.55$ arcmin, and a tidal radius $r_t = 8.16$ arcmin. It is very reddened, with $E(B-V) = 0.73$, $A_V = 2.26$, and $A_K = 0.23$ (Barbuy et al. 1998). Particularly relevant for this work is the distance of the cluster. We adopt a distance of 6.0 kpc for this cluster following Alves-Brito et al. (2006), as listed in the 2010 version of Harris (1996) catalog, noting that the distance uncertainty adds to the total error budget. We observe the cluster horizontal branch (HB) at $K_s = 12.5$ (Figure 3), which is consistent with this distance measurement.

Zoccali et al. (2001) measured a relative proper motion of NGC 6553 with respect to the bulge of $\mu_\alpha = 5.89$ and $\mu_\delta = 0.42$ mas/yr. This gives a relative mean proper motion difference

---

9 http://www.aavso.org/sites/default/files/images/LTGKper.gif
between bulge and cluster stars in the sky of 5.9 mas/yr. That would be the expected mean relative proper motion of the bulge source and the lens if the latter is a globular cluster member. Of course, the large bulge velocity dispersion can result in a larger or smaller actual relative proper motion.

The source star in particular (with $K_s = 13.5, J - K_s = 1.0$ at the baseline) is redder than the RGB of the globular cluster, consistent with a bulge giant. The source is also fainter than the bulk of the bulge red clump stars. If the source is a red clump giant star, it must be located on the far side of the bulge, at $D_s \approx 9$ kpc.

The field is very crowded and contains numerous bulge giants, and therefore membership of the lens to the cluster cannot be unambiguously secured. Luckily the VVV Survey images cover a large area (1.5 sqdeg), and we can measure the background contamination. At the distance of 3.5 arcmin from the center of the cluster, we estimate that roughly 20% of the stars per unit area are cluster members. However, that may or may not apply to the distribution of heavy remnants. In contrast, the microlensing event discussed by Yee et al. (2013) was located 6.7 arcmin away from this cluster, where the cluster stellar density is 6%, based on which they estimated that there is only 18% probability that their lens is a cluster member. Following their procedure we estimate that there is roughly 50% probability that the lens, located 3.5 arcmin from NGC 6553, actually belongs to the cluster.

4. THE CANDIDATE BH LENS

The dark microlensing events toward the bulge (i.e., with no light from the lens) that have long-duration (>100 days) may be due to massive stellar remnants. However, the masses based
on timescales are statistical mass estimates. Long-duration events can also be due to slow-moving, low-mass objects. This makes the present event particularly interesting, since an Einstein diameter crossing time of $t = 103$ days (Bennett et al. 2002), may be due to a relatively massive lens, such as a heavy non-luminous remnant (NS or BH).

Because of the position of the source star in the CMD (Figure 3) we can assume that it is located in the Galactic bulge. Under this assumption, we consider two scenarios: In the first scenario the lens is a member of the globular cluster NGC 6553. In this case we can estimate the lens mass (cf. Paczynski 1994, 1996), because we know the distance and the proper motion of the cluster.

We have fitted different possibilities considering different distances to the source star. The mass determination is uncertain due to the unconstrained $\mu_{rel}$, due also to the considerable bulge line of sight depth (Nataf et al. 2013). The most likely source distance is where the density of bulge stars peaks along the line of sight, i.e., $D_s = 8$ kpc. In this case, assuming $D_s = 6$ for the lens, we obtain a lens mass $M_\ell = 3.5 \pm 0.1 M_\odot$ (using relative transverse velocity $220 \text{ km s}^{-1}$), or $M_\ell = 2.0 \pm 0.1 M_\odot$ (using relative transverse velocity $168 \text{ km s}^{-1}$). If the source star is located in the far side of the bulge, at $D_s = 9$ kpc, we obtain a smaller lens mass, $M_\ell = 2.7 \pm 0.1 M_\odot$, and $M_\ell = 1.5 \pm 0.1 M_\odot$ for both cases, but still within the realm of the heavy remnant hypothesis. As discussed in Section 2, there are two equally good fits, one with a dark lens (case A with blending parameter $f = 1.0$), and another one with a significant contribution from an unresolved source (case B with $f = 0.62 \pm 0.20$). In the case of the first fit, if the lens is a member of NGC 6553, we estimate $M = 3.1 \pm 0.4 M_\odot$ and $M = 1.8 \pm 0.2 M_\odot$ for both cases, where the uncertainty is driven by the source distance and transverse motions. This fit then rules out other stellar remnants such as white dwarfs, and is more consistent with a NS or BH Stellar remnant.

Even though we claim priority for recognising this as a BH candidate, this event was independently found by OGLE\textsuperscript{10} as event OGLE-2012-BLG-0548. We would like to note that the reported OGLE microlensing parameters agree quite well with the ones derived solely from VVV photometry.

Bennett et al. (2002) estimate that the mean mass for six microlensing parallax events that they study is $2.7 M_\odot$, suggesting that they are BH candidates because they surpass the Chandrasekhar mass of $1.4 M_\odot$, being even larger than the allowed maximum NS mass of $2.0 M_\odot$. Interestingly, the mass we measure for the lens studied here is similar to the mean mass estimated for the six long timescale microlenses studied by Bennett et al. (2002).

This is an interesting case to study, because if the lens is so massive and old, it should be located close to the center of the cluster. It is unexpected to find a heavy stellar remnant at a distance of about 6 core radii from the cluster center so long after its formation. For example, the populations of millisecond pulsars and LMXBs in globular clusters tend to be among the most radially concentrated, and it is not clear why this BH did not sink into the globular cluster center through dynamical friction (e.g., Heinke et al. 2005).

As another point, we note that XMM source \#27 in NGC 6553 from Guillot et al. (2011) located at R.A. (2000) = 18:09:21.67, decl.(2000) = −25:57:31.6 is the closest X-ray source to the position of the microlensing event located about 2 arcmin away. Based on the existing data, however, it appears unlikely that XMM source \#27 corresponds to radiation from this candidate BH, as expected if it is accreting gas from the interstellar medium or the wind of a companion star (e.g., Agol et al. 2002).

In the second scenario that we consider, the lens is not a member of the globular cluster NGC 6553. In this case the distance to the lens is unknownd and its mass is not well constrain at all. However we can make some assumptions to visualize possible solutions. If we consider the distance of the bulge for the source, a long timescale can be obtained for a low-mass star as lens only if this lens is located at a few kpc from the Sun. For a source at a distance of $D_S = 8$ kpc, and assuming that the lens is located at $D_L = 3, 4, and 5$ kpc with a typical disk velocity of $V = 220 \text{ km seg}$ we estimate: $M_\ell = 2.8 M_\odot$, $M_\ell = 2.6 M_\odot$, $M_\ell = 2.8 M_\odot$, respectively. Instead, for a source at a distance of $D_S = 9$ kpc, and a lens at $D_L = 3, 4, and 5$ kpc we estimate: $M_\ell = 2.6 M_\odot$, $M_\ell = 2.3 M_\odot$, $M_\ell = 2.3 M_\odot$, respectively.

This case would favor the second fit more, with significant blending from an unresolved source. However, this is interesting because the inferred masses are large for a typical disk main sequence star. If the lens is a main sequence star, it should be bright enough and should have been observed.

5. CONCLUSIONS

We have re-discovered a microlensing event in the field of the globular cluster NGC 6553. Because the distance of this cluster is well known ($D = 6.0$ kpc), and the CMD suggests that the source is likely a bulge red giant at $D_s = 8–9$ kpc, we can solve for the mass of the lensing object if we assume this is a cluster member. Simply using Equation (15) of Paczynski (1996) results in a lens mass of $M = 1.5–3.5 M_\odot$ consistent with a heavy remnant.

There is another equally good fit to the microlensing light curve, with significant blending from an unresolved source. However, we note that combining the optical and IR data from OGLE and VVV, the microlensing color can be more precisely measured, and it appears to be essentially similar to the baseline color, meaning that the blending is really small, or alternatively that the lens has exactly the same color as the source. Proper motion measurements are warranted in this case, and combining VVV and OGLE data would greatly increase the precision of the parallax measurement and will be of great importance to better constrain the mass of this object. The alternative scenario of a more nearby disk main sequence star lensing a distant bulge giant cannot be ruled out, but also yields a rather massive lens ($2.3–2.8 M_\odot$). Even though we cannot rule out this possibility, it appears to be less likely because in this case the lens would be detectable as a bright blue star.

We can make specific predictions if the lensing object is a cluster member: the lens should eventually move away from the source because the relative proper motion of this globular cluster is relatively large, and then be detected if it is a stellar object, or remain invisible if it is an isolated BH. This method is the best way to confirm the microlensing nature of the event.

\textsuperscript{10} Reported online at: http://ogle.astrouw.edu.pl/ogle4/ews/2012/ews.html.
In the present case, the source-lens separation can reach the 60 mas range within 10 years (Zoccali et al. 2001), and the lensing star should be detected with high-resolution images (with HST or AO cameras) if it is not a BH in the cluster. In this sense, immediate high resolution K-band measurements using AO are desirable in order to provide a reference image for subsequent detection of the lens.

If membership to the cluster is confirmed with follow-up observations, this would not only be the only known stellar mass BH in a globular cluster, an important object to validate stellar evolution theory, but also the oldest BH known. This discovery opens up some interesting questions, like what is the mass distribution of globular cluster BHs produced by the death of ancient massive stars, why this BH did not sink into the globular cluster center through dynamical friction, how many of these low-mass BHs can be present in globular clusters, and how much these objects contribute to the total mass budget of dark remnants in the Milky Way and the universe.

We thank the referee A. Gould for very useful suggestions that improved our paper. We gratefully acknowledge use of data from the ESO Public Survey programme ID 179.B-2002 taken with the VISTA telescope, and data products from the Cambridge Astronomical Survey Unit, and funding from the BASAL CATA Center for Astrophysics and Associated Technologies MAS from the Ministry of Economy, Development, and Tourism through Programa Iniciativa Científica Milenio grant awarded to the Millennium Institute of Astrophysics MAS from the Ministry of Economy, Development, and Tourism through Programa Iniciativa Científica Milenio grant awarded to the Millennium Institute of Astrophysics. We warmly thank the ESO Paranal Observatory staff for performing the observations and Mike Irwin, Eduardo Gonzalez-Solares, and Jim Lewis at CASU for pipeline data processing support.

REFERENCES

Agol, E., Kamionkowski, E., Koopmans, L. V. E., & Blandford, R. D. 2002, ApJ, 576, 131
Alonso-García, J., Dekany, I., Catelan, M., et al. 2015, AJ, 149, 99
Alonso-García, J., Mateo, M., Sen, B., et al., 2012, AJ, 143, 70
Alves-Brito, A., Barbuy, B., Zoccali, M., et al. 2006, A&A, 460, 269
Barbuy, B., Bica, E., & Ortolani, S. 1998, A&A, 333, 117
Bennett, D. P., Becker, A. C., Quinn, J. L., et al. 2002, ApJ, 579, 639
Catelan, M., Dekany, I., Hempel, M., & Minniti, D. 2013, BAAA, 56, 153
Emerson, J. P., Irwin, M. J., Lewis, J., et al. 2004, Proc. SPIE, 5493, 401
Gould, A., & Salim, S. 1999, ApJ, 524, 794
Gould, A., & Yee, J. C. 2014, ApJ, 784, 64
Guillot, S., Rutledge, R. E., Brown, E. F., Pavlov, G. G., & Zavlin, V. E. 2011, ApJ, 738, 129
Hambly, N. C., Mann, R. G., Bond, I., et al. 2004, Proc. SPIE, 5493, 423
Harris, W. E. 1996, AJ, 112, 1487
Heinke, C. O., Grindlay, J. E., Edmonds, P. D., et al. 2005, ApJ, 625, 796
Hempel, M., Minniti, D., Dekany, I., et al. 2014, Msngr, 155, 29
Irwin, M. J., Lewis, J., Hodgkin, S., et al. 2004, Proc. SPIE, 5493, 411
Mao, S. 2012, RAA, 12, 947
Minniti, D. 1995, AJ, 109, 1663
Minniti, D., Lucas, P. W., Emerson, J. P., et al. 2010, NewA, 15, 433
Nataf, D. M., Gould, A., Fouqué, P., et al. 2013, ApJ, 769, 88
Ortolani, S., Renzini, A., & Gilmozzi, R. 1995, Natur, 377, 701
Paczynski, B. 1994, AcA, 44, 235
Paczynski, B. 1996, ARA&A, 34, 419
Pietrukowicz, P., Kaluzny, J., Thompson, I. B., et al. 2005, AcA, 55, 261
Pietrukowicz, P., Minniti, D., Jetzer, Ph., Alonso-García, J., & Udalski, A. 2012, ApJ, 744, 18
Poindexter, S., Afonso, C., Bennett, D. P., et al. 2005, ApJ, 633, 914
Refsdal, S. 1964, MNRAS, 128, 295
Saito, R. K., Hempel, M., Minniti, D., et al. 2012, A&A, 537, 107
Schechter, P. L., Mateo, M., & Saha, A. 1993, PASP, 105, 1342
Sutherland, W., Emerson, J., Dalton, G., et al. 2015, A&A, 575, 25
Taylor, M. B. 2006, ASPC, 351, 666
Yee, J. C., Hung, L.-W., Bond, I. A., et al. 2013, ApJ, 769, 77
Zoccali, M., Renzini, A., Ortolani, S., Bica, E., & Barbuy, B. 2001, AJ, 121, 2638