Measurement of long-range angular correlations and azimuthal anisotropies in high-multiplicity $p+Au$ collisions at $\sqrt{s_{NN}} = 200$ GeV

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We present the first measurements of long-range angular correlations and the transverse momentum dependence of elliptic flow $v_2$ in high-multiplicity $p+$Au collisions at $\sqrt{s_{NN}} = 200$ GeV. A comparison of these results with previous measurements in high-multiplicity $d+$Au and $^3$He+$Au$ collisions demonstrates a relation between $v_2$ and the initial collision eccentricity $\varepsilon_2$, suggesting that the observed momentum-space azimuthal anisotropies in these small systems have a collective origin.
I. INTRODUCTION

The azimuthal momentum anisotropy of particle emission relative to the participant plane of the collision, as quantified by the Fourier coefficients $v_n$ of the final state particle yield, has long been considered evidence for the formation of a strongly interacting, fluid-like quark-gluon plasma (QGP) in A+A collisions [1]. Viscous hydrodynamics supports a picture in which the initial spatial distribution in energy density, both from intrinsic geometry and fluctuations, is propagated into the final state as anisotropies in momentum space. The success of hydrodynamics in describing various bulk observables of the QGP has lent credence to the notion of hydrodynamic flow as the main driver of the $v_n$ signal in heavy A+A collisions.

However, recent analyses of $d$+Au and $^3$He+Au collisions at $\sqrt{s_{NN}} = 200$ GeV [2–5] at the Relativistic Heavy-Ion Collider (RHIC), and $p$+Pb at $\sqrt{s_{NN}} = 5.02$ TeV, and $p$+$p$ collisions at $\sqrt{s_{NN}} = 2.76, 5.02, 7$, and $13$ TeV [6–12] at the Large Hadron Collider (LHC) have demonstrated the existence of the same kind of azimuthal anisotropy signals commonly interpreted as evidence of collective behavior in larger systems. Notably, a feature known as the ridge has been observed, consisting of a near-side (i.e., at small relative azimuth) enhancement in the long-range (i.e., at large relative pseudorapidity) azimuthal two-particle correlation. From these correlations, substantial elliptic ($v_2$), and triangular ($v_3$) flow coefficients have been measured in these systems.

Although these observations seem to support the idea of QGP formation in small systems, it is not clear that hydrodynamic expansion would translate initial geometry into final state momentum anisotropy in this regime, where the formed medium is expected to be short-lived. Other explanations have been put forth, including initial state effects from glasma diagrams [13], color recombination [14], and partonic scattering in transport models [15–17]. Transport model calculations, as well as those from hydrodynamics, involve the translation of initial geometry into momentum space via final state interactions. Transport models describe interactions between well defined particles in kinetic theory, while hydrodynamics involves fluid elements. In contrast, glasma diagrams take momentum-space domains as a starting point, resulting in momentum correlations without any final-state interactions. In this initial momentum-space domain picture, the correlations averaged over the event should become weaker in going from $p$+Au, to $d$+Au, to $^3$He+Au as the average is taken over a larger number of domains, thus diluting the strength of the correlation effect. There is no direct correspondence with the initial geometric eccentricity in this picture. A key experimental test to resolve the issue consists in varying the initial geometry of the system to analyze the extent to which it carries into the final state [18].

The PHENIX collaboration has actively pursued this course of study by analyzing data from intrinsically elliptic ($d$+Au) [2,3] and triangular ($^3$He+Au) [4] collision systems at $\sqrt{s_{NN}} = 200$ GeV. Viscous hydrodynamics followed by a hadron cascade has been found to accurately reproduce the measured $v_n$ [2,4,19–21] for these systems.

This article completes the above suite of studies by presenting two-particle correlations and the transverse momentum ($p_T$) dependence of $v_2$ for central $p$+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. In small system collisions, the term central refers to events with high-multiplicity and the correlation with actual impact parameter is weak. These results are compared to those from $d$+Au and $^3$He+Au collisions, as well as to available theoretical calculations. We apply the same analysis procedure to all three systems in the same centrality class, to provide a controlled comparison from which to draw conclusions.

II. METHODS

A detailed description of the PHENIX detector can be found in Refs. [22, 23]. For this analysis, charged particles were reconstructed with the two central arm spectrometers, consisting of drift chambers and multi-wire proportional pad chambers (PC), each covering $|\eta| < 0.35$ in pseudorapidity and $\pi/2$ in azimuth. Drift chamber tracks are matched to hits in the third (outermost) layer of the PC, thus limiting the contribution of tracks from decays and photon conversions. The beam-beam counters (BBC) comprise two arrays of 64 quartz radiator Čerenkov detectors, located longitudinally $\pm 1.44$ m away from the center of the interaction region (IR), covering $3.0 < |\eta| < 3.9$ and $2\pi$ in azimuth. The forward vertex detector (FVTX) is a silicon detector comprising two identical end-cap assemblies symmetrically located in the longitudinal direction around the IR, covering the pseudorapidity range $1.0 < |\eta| < 3.0$. It uses hit clus-
ters to detect charged particles with an efficiency greater than 95%. The arms of the BBC and FVTX in the Au-going direction (i.e., $\eta < 0$) are designated as the south arms and styled BBC-S and FVTX-S, respectively. We use the south arm of each of these two detectors to determine the flow event plane. In addition, the $z$-vertex of the collision is found using event timing information from both arms of the BBC. In this analysis, a $\pm 10$ cm cut on the collision $z$-vertex was applied. We compare $p+Au$ correlation functions with those measured in $p+p$, as described in detail in Ref. [4].

The $p+Au$ data set for this analysis was collected during the 2015 data-taking run at RHIC. It comprises 0.84 billion minimum bias (MB) triggered events and 1.4 billion high-multiplicity (HM) triggered events. The MB trigger is defined as a coincidence in the same event between the BBC detectors [24] in the Au-going and $p$-going directions, requiring at least one photomultiplier tube (PMT) firing in each; in this way $84\pm 4\%$ of the total inelastic $p+Au$ cross section is captured. The HM trigger is based on the MB trigger, but imposes the additional requirement of more than 35 photomultiplier tubes firing in the BBC-S. Events that satisfy this trigger condition correspond roughly to the 5% most central event class. The use of this trigger allows us to increase our central event sample size by a factor of 25.

In this analysis, we select the 0%–5% most central $p+Au$ events, where centrality classes are defined by the percentiles of the total multiplicity measured in the BBC-S for MB events, following the procedure documented in Ref. [25]. Fig. 1(a) shows the measured distribution of BBC-S charge for the MB and HM trigger event samples, where the latter has been scaled to match the MB distribution. We model the BBC-S charge deposition using a Monte Carlo Glauber model with fluctuations following a negative binomial distribution. The resulting distribution is shown as a histogram, with the colored areas representing various centrality classes. Fig. 1(b) shows the ratio of the measured distribution to the MC Glauber calculation for MB events. The inefficiency observed below 10 units of charge indicates the MB trigger turn-on.

The initial geometry of events in various centrality selections is characterized using a standard Monte Carlo Glauber approach, where nucleon coordinates are smeared by a two-dimensional Gaussian of width $\sigma = 0.4$ fm. In this model, initial state eccentricity $\varepsilon_2$ is computed from initial Gaussian-smereared nucleon coordinates, as shown in Eq. 1.

$$\varepsilon_2 = \sqrt{\langle r^2 \cos(2\phi) \rangle^2 + \langle r^2 \sin(2\phi) \rangle^2} / \langle r^2 \rangle$$

In the above equation, $r$ is the radial nucleon position relative to the centroid of the participants, and $\phi$ is the nucleon azimuthal angle. The results of this Glauber characterization of the initial geometry are shown in Table I. The quantities characterizing the event geometry are the same within uncertainties for both the MB and HM event samples.

III. RESULTS

Long-range angular correlations are constructed between charged tracks in the PHENIX central arms at a given $p_T$, and charge deposited in the BBC-S PMTs, for central $p+Au$ collisions. The distribution of these track-PMT pairs is constructed over relative azimuth as given in Eq. 2, with the normalized correlation function given by Eq. 3, following Ref. [26]:

![Graph and Table](image-url)
The weights $w_{\text{PMT}}$ for each pair correspond to the charge in the PMTs comprised in that particular pair. The signal distribution $S$ is constructed from pairs in the same event. The mixed distribution $M$ is constructed using pairs from different events in the same centrality class and collision vertex bin. Ten equally sized bins are used within the range of $|z| < 10$ cm in the event mixing.

The resulting correlation functions for three track $p_T$ selections are shown in Fig. 2. Each one is fit with a four-term cosine Fourier series, $C(\Delta \phi) = \sum_{n=1}^{4} 2c_n \cos(n \Delta \phi)$. The magnitude of the second harmonic $c_2$ as a function of $p_T$ is shown with red circles in Fig. 3 panel (a). The contribution of elementary processes (e.g., jet fragmentation, resonance decays, and momentum conservation effects) to the measured $c_2$ in $p+Au$ can be estimated quantitatively using previously published $c_2$ data from $p+p$ at the same collision energy [4], scaled down by an appropriate factor to account for the higher multiplicity in $p+Au$. We choose the scale factor to be the ratio of the total charge deposited in the BBC-S (i.e., $Q^{\text{BBC-S}}$) in $p+p$ relative to $p+Au$, as shown in Eq. 3, because we can think of a $p+Au$ event as the superposition of $N$ independent nucleon-nucleon collisions, where the correlation strength from a single collision scales inversely with $N$.

$$S(\Delta \phi, p_T) = \frac{d(w_{\text{PMT}}N_{\text{Same event}} - \text{PMT})}{d\Delta \phi}, \quad (2)$$

$$C(\Delta \phi, p_T) = \frac{S(\Delta \phi, p_T)}{M(\Delta \phi, p_T)} \int_0^{2\pi} M(\Delta \phi, p_T) d\Delta \phi. \quad (3)$$

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$$c_2^{p+Au\text{elementary}}(p_T) \simeq c_2^{p+p}(p_T) \frac{\langle Q^{\text{BBC-S}} \rangle_{p+p}}{\langle Q^{\text{BBC-S}} \rangle_{p+Au}}. \quad (4)$$

The scaled down reference $c_2$ is shown as blue squares in Fig. 3, panel (a). The ratio of $c_2$ in the scaled-down $p+p$ reference to $p+Au$ is shown in panel (b). From this ratio, it can be seen that the relative correlation strength in $p+Au$ from elementary processes is at most 23% at the highest $p_T$. Because this procedure constitutes an approximation to quantify the nonflow correlation strength, which may be affected by other factors not considered in this analysis, we do not subtract it from the total signal, treating it instead as a source of systematic uncertainty. Even though the $p+Au$ and the $p+p$ baseline data were collected in different years, where potential changes in detector performance could affect our results, we verified that using $p+p$ data from various run periods has an effect of at most 3% on the calculated nonflow contribution.

It is noteworthy that, unlike in $d+Au$ [20] and $^3\text{He}+\text{Au}$ [26] collisions at the same centrality, the long-range angular correlations in $p+Au$ do not exhibit a discernible near-side peak, yet possess a nonnegligible second harmonic component. The nonflow contribution from elementary processes and momentum conservation becomes more dominant as the system size and particle multiplicity decrease. This results in a larger $|c_1|$ and thus a smaller $|c_2/c_1|$ ratio, and hence in a less discernible near-side peak in $p+Au$.

Having quantified the strength of the correlations from elementary processes, we determine the second Fourier coefficient $v_2$ of the single-particle azimuthal distributions, which is typically associated with collective elliptic flow, using the event plane method as described in Ref. [27]. Namely, we measure

$$v_2(p_T) = \frac{\langle \cos 2(\phi_{\text{Particle}}(p_T) - \Psi^{\text{FVTX-S}}_2) \rangle}{\text{Res}(\Psi^{\text{FVTX-S}}_2)} \quad (5)$$

for charged hadrons at midrapidity, where the second order event plane $\Psi^{\text{FVTX-S}}_2$ is determined for every event using the FVTX-S detector. Its resolution $\text{Res}(\Psi_2)$ is computed using the standard three-subevent method [27], correlating measurements in the BBC-S, FVTX-S, and the central arms. This results in $\text{Res}(\Psi^{\text{FVTX-S}}_2) = 0.171$. It is also possible to measure the event plane using the BBC-S. In that case, we obtain a lower resolution $\text{Res}(\Psi^{\text{BBC-S}}_2) = 0.062$, and $v_2$ values that differ from the FVTX-S measurement by approximately 3%. The very good agreement of $v_2$ measured using the BBC-S and FVTX-S event planes is interesting, because the pseudorapidity gaps relative to the midrapidity tracks are $|\Delta \eta| > 2.65$ and $|\Delta \eta| > 0.65$, respectively.

The main sources of systematic uncertainty in the $v_2(p_T)$ measurement are: (1) track background from photon conversion and weak decays, whose magnitude we determine at 2% relative to the measured $v_2$ by varying the spatial matching windows in the PC3 from $3\sigma$ to $2\sigma$; (2) Multiple collisions per bunch crossing (i.e., event pile-up) that are observed to occur at an average rate of $8\%$ in the $0\%$–$5\%$ central $p+Au$ collisions. Low luminosity and high-luminosity subsets of the data were analyzed separately and the systematic uncertainty in the $v_2(p_T)$ value is determined to be asymmetric $+5\%$, because the $v_2$ values were found to decrease in the events that contain a larger fraction of pile-up; (3) Non-flow correlations from elementary processes that enhance the $v_2$ values, whose contribution we estimate from Fig. 3, assigning a $p_T$-dependent asymmetric uncertainty with a maximum value of $+0.23$% for the highest $p_T$ bin. This can be compared to the corresponding $+0.3$% [3] and $+0.07$% [4] systematic uncertainties in $d+Au$ and $^3\text{He}+\text{Au}$ collisions, respectively; (4) The asymmetry between the east ($\pi/2 < \phi < 3\pi/2$) and west ($-\pi/2 < \phi < \pi/2$) acceptance of the detectors due to an offset of $3.6$ mrad between the colliding beams and the longitudinal axis of PHENIX, necessary for running $p+Au$ at the same momentum per nucleon. We applied a corresponding counter-rotation to every central arm track and detector element in the FVTX and BBC, which were also reweighted to restore their uniformity in azimuth. We assign a value of 5% for this systematic uncertainty by taking the difference of $v_2$ as measured independently in the
FIG. 2. Long-range angular correlations $C(\Delta \phi, p_T)$ constructed with central arm tracks and BBC-S PMT pairs, in 0%–5% central $p$+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. From left to right, correlations are shown for various track $p_T$ categories: (a) 0.5–1.0 GeV/$c$, (b) 1.0–2.0 GeV/$c$, and (c) 2.0–3.0 GeV/$c$. We fit each correlation with a four-term cosine Fourier series. The harmonic $c_1$ is shown as a short-dashed line; $c_2$, as a dotted line; $c_3$, as a dash-dot line; $c_4$, as a long-dashed line. The total fit is shown as a solid line.

FIG. 3. (a) The second order harmonic coefficients $c_2(p_T)$ for long range angular correlations in 0%–5% $p$+Au collisions, as well as for MB $p$+$p$ collisions. The latter are scaled down by the factor $\left(\sum Q^{BBC-S}_{p+p} / \sum Q^{BBC-S}_{pAu}\right)_{pAu}$. (b) The ratio of the two harmonics is plotted with the corresponding statistical errors.

Table II summarizes all these systematic uncertainties, categorized by type:

- (A) point-to-point uncorrelated between $p_T$ bins,
- (B) point-to-point correlated between $p_T$ bins,
- (C) overall normalization uncertainty in which all

east and the west arms after applying the above corrections; (5) The difference in the $v_2(p_T)$ values when measured independently using the BBC-S and FVTX event planes, which we observe to differ by ±3%.

Table II summarizes all these systematic uncertainties, categorized by type:

| Source                        | Systematic Uncertainty | Type |
|-------------------------------|------------------------|------|
| Track Background              | 2.0%                   | A    |
| Event Pile-up                 | $^{+4}_{-0}$%           | B    |
| Non-Flow                      | $^{-23}_{+0}$%          | B    |
| Beam Angle                    | 5.0%                   | C    |
| Event-Plane Detectors         | 3%                     | C    |

The resulting $v_2$ measurement for $p$+Au, compared to $d$+Au [3] and $^3$He+Au [4] in the same 0%–5% centrality class, is shown in Fig. 4. The $d$+Au data, as presented in Ref. [3], did not include nonflow contributions in its systematic uncertainties, which are now accounted for in the systematics shown in Fig. 4. In all cases, there is a substantial $v_2$ that rises with $p_T$. It is notable that the $v_2$ values for $d$+Au and $^3$He+Au are consistent within uncertainties, as are their eccentricities $v_2$ listed in Table I. The $p$+Au collisions have a significantly lower $v_2$ and a correspondingly lower calculated $v_2$. At the same time, the ordering of $v_2$ from $p$+Au, to $d$+Au, to $^3$He+Au also follows the expected increasing order of particle multiplicity. In the case of $d$+Au and $^3$He+Au, for the 0%–5% most central events, the published values for midrapidity charged particle density are $dN_{ch}/dy = 20.8 \pm 1.5$ and $26.3 \pm 1.8$, respectively [28]. This quantity has not yet been measured in $p$+Au collisions.
IV. DISCUSSION

Also shown in Fig. 4 are $v_2$ calculations for each system from the sonic hydrodynamic model [29], which incorporates standard Monte Carlo Glauber initial conditions followed by viscous hydrodynamics with $\eta/s = 0.08$, and a transition to a hadronic cascade at $T = 170$ MeV. It is notable that these calculations for each system are matched to the charged particle density at midrapidity, with the exact values for 0%-5% centrality of 10.0, 20.0, and 27.0, for $p+Au$, $d+Au$, and $^3He+Au$ collisions, respectively [29]. Again, note that $dN_{ch}/d\eta$ has not been measured for $p+Au$, and that the value of 10.0 was extrapolated from measurements in the other two systems [29]. We thus see that the calculation includes both the geometry-related change in eccentricity and the relative collision multiplicity. In all cases, a good agreement is seen within uncertainties between the data and the calculation. These observations strongly support the notion of initial geometry, coupled to the hydrodynamic evolution of the medium as a valid framework to understand small system collectivity.

To further explore this idea, we divide the $v_2$ curves by their corresponding $\varepsilon_2$ from Table I, attempting to establish a scaling relation between the two quantities. Fig. 5 shows that the ratios do not collapse to a common value. As expected, this behavior is also reproduced by the sonic calculation, because both data and calculation are divided by the same $\varepsilon_2$ values. The lack of scaling in the sonic calculation can be understood from $d+Au$ events where the neutron and proton from the deuterion projectile are far separated and create two hot spots upon impacting the Au nucleus. These events have a large $\varepsilon_2$, but can result in small $v_2$ if the two hot spots evolve separately, never combining within the hydrodynamic time evolution. This effect is present in the $d+Au$ and $^3He+Au$ systems, and lowers the average $v_2/\varepsilon_2$ as detailed in Ref. [18].

Figure 6 shows $v_2(p_T)$ for 0%-5% central $p+Au$, $d+Au$, and $^3He+Au$ events, along with theoretical predictions available in the literature, most notably from hydrodynamics with Glauber initial conditions (SONIC [29] and SUPERSONIC [19]), hydrodynamics with IP-Glasma initial conditions [30], and A-Multi-Phase-Transport Model (AMPT) [31].

The SUPERSONIC model uses the same prescription for initial conditions, hydrodynamic expansion, and hadronic cascade as SONIC, yet additionally incorporates pre-equilibrium dynamics with a calculation in the framework of the AdS/CFT correspondence [32-34]. These two models agree well with the data within uncertainties, supporting the idea of initial geometry as the driver of the $v_n$ signal. Furthermore, this illustrates how these results impose useful constraints to reduce the number of free parameters of the model, because many such parameters must be identical across systems, e.g., $\eta/s$, the transition temperature to a hadron cascade, and the Monte Carlo Glauber smearing of nucleon coordinates of $\sigma = 0.4$ fm.

Calculations using IP-Glasma initial conditions followed by viscous hydrodynamics have been successfully used to describe collectivity in A+A collisions [35]. It is notable that in these calculations the glasma framework is used only to determine the initial spatial configuration as input to hydrodynamics; there is no glasma diagram or momentum-domain physics incorporated, such that all of the collectivity arises from final-state interactions. When this framework is applied to small collision systems with $\eta/s = 0.12$ and $b < 2$ fm, as shown in Fig. 6, the calculation substantially overestimates the data for $d+Au$ and $^3He+Au$, while underestimating it for $p+Au$. This follows from the fact that IP-Glasma generates very circular initial conditions for $p+Au$, corresponding to very low $\varepsilon_2$ values; however, the presence of several hot spots in $d+Au$ and $^3He+Au$ result in IP-Glasma values for $\varepsilon_2$ more comparable to those from Glauber. This is shown in Table III.

| $\langle \varepsilon_2 \rangle$ | $p+Au$ | $d+Au$ | $^3He+Au$ |
|-------------------------------|--------|--------|-----------|
| Glauber                        | 0.23 ± 0.01 | 0.54 ± 0.04 | 0.50 ± 0.02 |
| IP-Glasma                      | 0.10 ± 0.02 | 0.59 ± 0.01 | 0.55 ± 0.01 |
The estimated magnitude is accounted for in the asymmetric systematic uncertainties. The data points shown include nonflow contributions, whose corresponding eccentricity $\varepsilon$ is obtained from Glauber calculations, compared to the values of the initial Glauber geometry, and thus have very similar eccentricities to those given in Table I. Using the initial Glauber geometry information to compute $v_2$ relative to the participant plane [17] yields results that agree reasonably well with the data below $p_T \approx 1$ GeV/c, yet underpredict them at higher $p_T$. It is noteworthy that despite the very different physics of AMPT compared to the other models, it has successfully been applied to a variety of systems at RHIC and the LHC. See, for example, Refs. [16, 17, 43, 44].

Finally, AMPT combines partonic and hadronic scattering in a single model. Central AMPT events with impact parameter $b < 2$ have a midrapidity $dN_{ch}/dy$ at 8.1, 14.8, and 20.7 for $p+Au, d+Au$, and $^3He+Au$, respectively. These were generated with the same Monte Carlo Glauber initial conditions used to characterize event geometry, and thus have very similar eccentricities to those given in Table I. Using the initial Glauber geometry information to compute $v_2$ relative to the participant plane [17] yields results that agree reasonably well with the data below $p_T \approx 1$ GeV/c, yet underpredict them at higher $p_T$. It is noteworthy that despite the very different physics of AMPT compared to the other models, it has successfully been applied to a variety of systems at RHIC and the LHC. See, for example, Refs. [16, 17, 43, 44].

V. SUMMARY

We have presented results on azimuthal anisotropy and elliptic flow in central $p+Au$ at $\sqrt{s_{NN}} = 200$ GeV, compared with $v_2$ in $d+Au$ and $^3He+Au$ collisions. These results impose strong constraints on any model attempting to describe small system collectivity, whether by the formation of strongly interacting hot nuclear matter, or other mechanisms. We observe an imperfect scaling of $v_2$ with $\varepsilon$, well reproduced by hydrodynamics, providing strong evidence for initial geometry as the source of final-state momentum anisotropy in these systems. This disfavors other explanations based on initial-state momentum space domain effects. Further insight into the nature of small system collectivity can be gained by analyzing the centrality and collision energy dependence of $v_2$, and will be the subject of future studies.

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FIG. 6. Transverse momentum dependence of $v_2$ in central 0%-5% (a) $p$+Au, (b) $d$+Au, and (c) $^3$He+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. Theoretical calculations from (solid [gray] curve) AMPT, (central [orange] band) SONIC, (top [blue] band) superSONIC, and (dot-dashed [magenta] curves) IPGlasma+Hydro are shown in each panel. Note that the data points shown include nonflow contributions, whose estimated magnitude is accounted for in the asymmetric systematic uncertainties.

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