Molecular Reconnaissance of the $\beta$ Pictoris Gas Disk with the SMA: A Low HCN/(CO+CO$_2$) Outgassing Ratio and Predictions for Future Surveys

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Abstract

The exocometary origin of CO gas has been confirmed in several extrasolar Kuiper belts, with CO ice abundances consistent with solar system comets. We here present a molecular survey of the $\beta$ Pictoris disk with the Submillimeter Array (SMA), reporting upper limits for CN, HCN, HCO$^+$, N$_2$H$^+$, and H$_2$CO, as well as for H$_2$S, CH$_3$OH, SiO, and DCN from archival ALMA data. Non-detections can be attributed to rapid molecular photodissociation due to the A-star’s strong UV flux. CN is the longest lasting and most easily detectable molecule after CO in this environment. We update our nonlocal thermodynamic equilibrium excitation model to include UV fluorescence, finding it plays a key role in CO and CN excitation, and we use it to turn the SMA CN/CO flux ratio constraint into an upper limit of $<2.5\%$ on the HCN/(CO+CO$_2$) ratio of outgassing rates. This value is consistent with, but at the low end of, the broad range observed in solar system comets. If sublimation dominates outgassing, then this low value may be caused by decreased outgassing for the less volatile molecule HCN compared to CO. If instead UV photodesorption or collisional vaporization of unbound grains dominates outgassing, then this low ratio of rates would imply a low ice abundance ratio, which would in turn indicate a variation in cometary cyanide abundances across planetary systems. To conclude, we make predictions for future molecular surveys and show that CN and HCN should be readily detectable with ALMA around $\beta$ Pictoris for solar-system-like exocometary compositions.

Key words: circumstellar matter – comets: general – molecular processes – planetary systems – stars: individual ($\beta$ Pictoris) – submillimeter: planetary systems

1. Introduction

Sensitive searches with the Atacama Large Millimeter/submillimeter Array (ALMA) are steadily adding to the number of disks with dust levels typical of debris disks but hosting detected CO gas, now comprising 15 systems (Zuckerman et al. 1995; Moór et al. 2011, 2015, 2017; Dent et al. 2014; Greaves et al. 2016; Lieman-Sifry et al. 2016; Marino et al. 2016, 2017; Matrà et al. 2017b). All but two of these are relatively young ($\sim$10–100 Myr old), which would naively suggest that the presence of CO is related to the protoplanetary era of disk evolution. However, the recent detections of CO around the 440 Myr old star Fomalhaut (Matrà et al. 2017b) and the 1–2 Gyr old star $\eta$ Corvi (Marino et al. 2017), as well as the tentative detection around the 125–130 Myr old eclipsing binary HD23642 (Péricaud et al. 2017), show that at least in some of the systems the CO cannot be primordial. Instead, the wide range of system ages advocates for CO replenishment through gas release from exocometary ices.

This exocomet scenario has now been confirmed as the origin of the observed CO gas in four systems, including relatively young stars $\beta$ Pictoris (Dent et al. 2014; Matrà et al. 2017a) and HD181327 (Marino et al. 2016), as well as Fomalhaut and $\eta$ Corvi. While the exact CO release mechanism itself remains unknown, the similarly clumsy CO and dust distributions in the disk around $\beta$ Pictoris suggest that collisions play an important role (Dent et al. 2014). A collisional cascade is expected to result in efficient gas release as long as the smallest grains blown out of the system by radiation pressure from the central star cannot retain their ice (Matrà et al. 2017b). In this case, assuming a steady state in both the collisional cascade and in the production and photodestruction of gas allows us to extract the CO ice fraction in exocomets from simple observables (Zuckerman & Song 2012; Matrà et al. 2015, 2017b). This is a particularly powerful tool to probe the bulk volatile composition of exocomets, allowing us to place solar system comets in the larger context of planetary systems around stars with different properties.

In the debris disk systems where an exocometary origin of CO has been confirmed (two A- and one F-type stars), measured CO mass fractions of exocomets are consistent with solar system comets (Marino et al. 2016; Matrà et al. 2017a, 2017b). This consistency suggests similar comet formation conditions in the original protoplanetary disks and the Solar Nebula. The next step in investigating this similarity requires us to both expand this sample of exocometary CO abundance measurements and probe relative ice abundances through detection of other molecules. As we discuss in this paper (Section 5), detection of other molecules can uniquely shed light on both the exocometary outgassing mechanism (where outgassing refers to any gas release process from solid bodies of any size) and the chemical history of cometary volatiles.

Here we present the first molecular survey of the exocometary gas disk around $\beta$ Pictoris. In Section 2, we describe new SMA and archival ALMA observations of CO, CN, HCN, HCO$^+$, N$_2$H$^+$, H$_2$CO, H$_2$S, CH$_3$OH, SiO, and DCN. The continuum and CO J = 2–1 detections with the SMA as well as SMA and ALMA upper limits for all other molecules are presented in Section 3. We interpret the observations with a steady-state exocometary release model in
Section 4. In particular, we focus on CN and CO as the longest lived observable gas-phase species in the disk, and we describe the connection between the constraint on the observed CN/CO flux ratio upper limit and an upper limit in the 2.17 GHz continuum image from the same 2014 data set, by measuring the centroid of continuum emission and spatially shifting the image to ensure that this centroid lies at the expected stellar location.

2. Observations

2.1. SMA

We observed the β Pictoris debris disk with the Submillimeter Array (SMA) on Maunakea, Hawaii, in two tracks in a compact antenna configuration to search for line emission from a suite of molecular species. Table 1 provides a summary of the observational parameters. The first track was obtained on 2014 November 11 using seven antennas. The ASIC correlator was configured with 128 channels (0.8125 MHz spacing) in each of 48 chunks that together spanned ±(4–8) GHz from an LO frequency of 221.654 GHz. In addition, the partly deployed SWARM correlator (operating at 8/11 speed) provided an additional two chunks of 16,384 channels each (0.8125/8 MHz spacing) that spanned ±(8–12) GHz from the LO frequency with a gain centered at 10 GHz of width 1.15 GHz. This setup was aimed at simultaneous coverage of spectral lines of CO and CN (USB).

The southern location of β Pictoris (decl. –51°) makes it a challenging target for the SMA, since it is available only at high air mass, rising above an elevation of 15° for only about 3 hr. However, for both of these tracks, the weather conditions were very good, with stable atmospheric phase and low opacity at 225 GHz as measured by the nearby tipping radiometer. The basic observing sequence consisted of a loop of 2 minutes each on the quasars J0522-364 and J0538-440 and 8 minutes on β Pictoris. Passband calibration was obtained with observations of a combination of available strong sources. The absolute flux scales for the two tracks were set using observations of Callisto and Uranus, with an estimated accuracy of 20%. All of the calibration was performed using the MIR5 software package. Continuum and spectral line imaging and clean deconvolution were done in the “miriad” package.

The 2014 data set presented a systematic astrometric offset of ∼2′.4 (a fraction of the 8′′ × 3′′ beam size) with respect to location of the star. We corrected this offset using the 274 GHz continuum image from the same 2014 data set, by measuring the centroid of continuum emission and spatially shifting the image to ensure that this centroid lies at the expected stellar location.

2.2. ALMA

We extracted ALMA Band 6 observations of β Pictoris from the archive (project number 2012.1.00142.S) in order to search for line emission from several additional molecular species. In summary, observations were performed between 2013 and 2015 with the 12 m array in a compact and extended configuration, as well as with the Atacama Compact Array (ACA), with total on-source times of 28, 114, and 50 minutes, respectively. We direct the reader to Matrà et al. (2017a) for a detailed description of the calibration and CO imaging procedures. Two of the spectral windows were set in frequency division mode and allowed us to test for the presence of spectral line emission from H$_2$S (22,0–21,1, 216.710 GHz), CH$_3$OH (5,4–4,2, 216.946 GHz), SiO (J = 5–4, 217.105 GHz), and DCN (J = 3–2, 217.239 GHz), as well as CO (J = 2–1, 230.538 GHz). We here repeated the imaging step for all molecules in the same way as previously done for the CO transition (Matrà et al. 2017a); this resulted in four line data sets with a native channel spacing of 488.281 kHz (corresponding to a resolution of 1.35 km s$^{-1}$ at the rest frequency of the SiO line). To allow direct comparison with CO (Section 3.2), we applied a taper to the visibilities in order to produce data cubes with exactly the same synthesized beam size (0′.30 × 0′.26, or 13.4 × 10.7 au at the distance of β Pictoris) and position angle (p.a., −83°9′) as the CO data set.

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### Table 1

| Parameter | 2014 Nov 11 | 2015 Dec 15 |
|-----------|-------------|-------------|
| No. antennas | 7           | 8           |
| 225 GHz rms noise | 0.07        | 0.04        |
| Pointing center | R.A. 05h47m17s, Decl. −51°30m59s (J2000) | |
| Min/max baseline | 6 to 67 m | 6 to 67 m |
| Gain calibrators | J0522-364 (2.7 Jy) | J0522-364 (4.9 Jy) |
|            | J0538-440 (1.7 Jy) | J0538-440 (1.5 Jy) |
| Passband calibrator | 3C84, Uranus | 3C84, Uranus |
| Flux calibrator | Callisto | Uranus |
| Spectral lines | | |
| Frequency | | |
| HCN J = 3–2 | CO J = 2–1 |
| 265.8643 GHz | 230.538 GHz |
| HCO$^+$ J = 3–2 | CN N = 2–1 |
| 267.5576 GHz | 226.8748 GHz |
| N$_2$H$^+$ J = 3–2 | (J = 5/2–3/2) |
| 279.51176 GHz | component |
| H$_2$CO J = 414 – 313 | 281.52693 GHz |
| Primary beam FWHM | 43′′ | 55′′ |
| Synthesized beam FWHM | 7′′7 × 3′′3, p.a. 12′′ | 8′′7 × 3′′7, p.a. −9′′ |
| rms noise (line images) | 0.09 Jy beam$^{-1}$ @ 265.9 GHz | 0.06 Jy beam$^{-1}$ @ 230.5 GHz |
|            | (for 0.92 km s$^{-1}$) | (for 1.06 km s$^{-1}$) |
| rms noise (continuum image) | 1.4 mJy beam$^{-1}$ | 0.57 mJy beam$^{-1}$ |

Note.

* For natural weighting plus a 3′′ Gaussian taper in the east–west direction.

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5 https://www.cfa.harvard.edu/~cqi/mircool.html
3. Results

3.1. SMA Continuum and CO $J = 2-1$ Detections

Continuum emission from dust within the β Pictoris disk is detected in both SMA data sets at 222 and 274 GHz (1.35 and 1.09 mm). Figure 1 (left) shows the SMA image with the highest signal-to-noise ratio ($S/N; 1.35$ mm), presenting a double-peaked morphology consistent with the 1.09 mm data set, as well as previous SMA 236 GHz (1.27 mm, Wilner et al. 2011) and ALMA 339 GHz (0.89 mm, Dent et al. 2014) data sets, interpreted as a belt viewed almost exactly edge-on. Flux density measurements from the SMA observations at 222 and 274 GHz are $21.0 \pm 3.0$ mJy and $25.9 \pm 6.4$ mJy, respectively (obtained by fitting a Gaussian to the visibilities at baselines shorter than $30 \lambda$). These values are consistent with the ALMA measurement at 339 GHz ($60 \pm 6$ mJy), given the large uncertainties and steep spectral index ($\alpha \sim 2.81$, Ricci et al. 2015). The previously reported SMA 236 GHz continuum measurement remains anomalously low ($13 \pm 1.4$ mJy), perhaps resulting from calibration challenges at very low elevations.

CO $J = 2-1$ emission is clearly detected in the SMA channel maps, centered around a velocity of $\sim 1.4$ km s$^{-1}$ with respect to the rest frequency of 230.538 GHz in the local standard of rest (LSR) reference frame. We created a moment 0 image (contours in Figure 1, right) by spectrally integrating the data cube within $\pm 7$ km s$^{-1}$ of the stellar velocity (the latter being consistent with the centroid velocity reported above). We used this image to create a spatial mask large enough to include all of the emission from the disk. Then, we applied this mask to the original data cube as a spatial filter; in other words, we spatially integrated emission within this mask. This produced the 1D spectrum shown in Figure 2 (top left, lilac line).

The CO line profile is spectrally resolved and appears asymmetric; the enhancement at blueshifted radial velocities is consistent with previous ALMA observations showing that the majority of CO emission originates in a clump on the southwest (SW) side of the edge-on disk, where this SW side is rotating toward Earth (Dent et al. 2014; Matrà et al. 2017a). This is...
confirmed by the moment 1 map (color map in Figure 1 right), which shows the line-of-sight velocity centroid of CO emission at spatial locations where the disk is detected (at the 4σ level). This centroid was obtained by fitting Gaussians to spectra at all spatial locations. Within the measurement uncertainties, the CO \( J = 2–1 \) line shape and integrated line flux are consistent with the previous ALMA measurements (see ALMA CO spectrum as the lilac line in Figure 2, top right, as well as CO line fluxes in Table 2).

### 3.2. Upper Limits from Molecular Survey: Spectrospatial Filtering Using CO as a Template

No significant signal is detected in the SMA data cubes created around the spectral location corresponding to the CN \( N = 2–1 \), \( J = 3/2 \) \( \pm \) \( 3/2 \) line (composed of the three blended \( F = 7/2 \) \( \pm \) \( 5/2 \) \( \pm \) \( 3/2 \), and \( 3/2 \) \( \pm \) \( 1/2 \) hyperfine transitions), HCN \( J = 3–2 \), HCO\(^+ \) \( J = 3–2 \), \( \text{N}_2\text{H}^+ J = 3–2 \), and \( \text{H}_2\text{CO} J = 4_1,4-3_1,3 \) lines. Similarly, no significant emission is observed in the ALMA data cubes around the \( \text{H}_2\text{S} 2_2,0-2_1,1 \), \( \text{CH}_3\text{OH} 5_{1,4}-4_{2,2} \), \( \text{SiO} J = 5–4 \), and DCN \( J = 3–2 \) lines.

To optimize detectability, we implement a spectrospatial filtering technique similar to that introduced in Matrà et al. (2015) and subsequently applied to achieve CO detections in the HD181327, \( \eta \) Corvi, and Fomalhaut debris disks (Marino et al. 2016, 2017; Matrà et al. 2017b). The method involves choosing a prior on the spectrospatial distribution of the gas emission, and using this prior to select pixel/channel combinations where emission is expected. This maximizes the signal-to-noise ratio by effectively removing noise-dominated pixels or channels.

We demonstrate this technique by applying it first to the CO \( J = 2–1 \) line already detected without need for filtering by both the SMA and ALMA. In practice, the process involves two steps. First, we apply spectral filtering by shifting all 1D spectra at each spatial location in the data cube by the negative of the centroid CO velocity displayed in the moment 1 map (Figure 1, right). This causes the spectra to align such that the bulk of the CO emission now lies at the stellar velocity at all spatial locations. Second, we apply spatial filtering by spatially integrating over the previously created mask covering the region where CO emission is detected. This produces the CO spectra shown in Figure 2 (top, red line) for the SMA (left) and ALMA (right) observations. This technique significantly improves the S/N of the detection with respect to the CO spectra directly extracted from the spectral image cube (lilac lines). The improvement is clearer for the ALMA data set since the line is better resolved both spectrally and spatially, increasing the number of spatial locations that are spectrally independent of one another. In other words, if the emission is better resolved spatially, then the spectral lines at each spatial location will be narrower, and the spectral shifting will produce a better alignment and consequential S/N boost.

For simplicity, we here assume emissions from all molecules have similar spectrospatial distributions of emission as observed for the CO molecule (though see caveats in Section 5.2). This allows us to use the observed CO emission as a template for the spectrospatial filtering technique. Figure 2 shows the resulting filtered spectra for all observed molecules. There are no significant detections of any molecular lines other than CO. We measure the filtered integrated flux upper limits by multiplying the filtered spectrum’s root mean square (rms, measured away from the line frequency) by the number of independent spectral channels covering the line width across which CO is detected. The 3σ limits derived are listed in Table 2. As this assumes that all molecules have the same spectrospatial distribution as CO, we also calculate upper limits in a more agnostic way by spatially integrating the unfiltered data cubes over regions where the millimeter continuum is detected, and spectrally integrating between \( \pm 5 \) km \( \text{s}^{-1} \) of the stellar velocity (values in parentheses in Table 2). Whether these are more or less stringent than the CO-filtered limits depends on both the on-sky area over which the continuum versus CO is detected, and on the spectral width of the CO line before versus after spectral filtering, which differs for the SMA and ALMA data sets (see top row in Figure 2).

### 4. Analysis

We investigate how to connect the line flux upper limits measured in Section 3 to exo cometary ice compositions relative to CO, the only molecular species detected so far in exo cometary gas disks. In particular, we aim to understand

| Species | Transition | Freq. (GHz) | Line Flux (Jy km s\(^{-1}\)) | Instr. | References |
|---------|------------|-------------|----------------------------|-------|------------|
| \( \text{H}_2\text{S} \) | \( 2_{2,0} - 2_{1,1} \) | 216.710 | \(< 0.10 (0.18) \) | ALMA | 1 |
| \( \text{CH}_3\text{OH} \) | \( 5_{1,4} - 4_{2,2} \) | 216.946 | \(< 0.11 (0.13) \) | ALMA | 1 |
| \( \text{SiO} \) | \( J = 5–4 \) | 217.105 | \(< 0.11 (0.16) \) | ALMA | 1 |
| DCN | \( J = 3–2 \) | 217.239 | \(< 0.13 (0.16) \) | ALMA | 1 |
| CO | \( J = 2–1 \) | 230.538 | 4.5 ± 0.5 | ALMA | 2 |
| | \( J = 3–2 \) | 345.796 | 5.8 ± 0.6 | ALMA | 2, 3 |
| CN | \( N = 2–1 \) | 226.875 | \(< 1.0 (1.2) \) | SMA | 1 |
| HCN | \( J = 3–2 \) | 265.886 | \(< 2.0 (1.4) \) | SMA | 1 |
| HCO\(^+ \) | \( J = 3–2 \) | 267.558 | \(< 1.5 (1.1) \) | SMA | 1 |
| \( \text{N}_2\text{H}^+ \) | \( J = 3–2 \) | 279.512 | \(< 1.7 (1.2) \) | SMA | 1 |
| \( \text{H}_2\text{CO} \) | \( J = 4_{1,4} - 3_{1,3} \) | 281.527 | \(< 1.6 (1.2) \) | SMA | 1 |

Note. For CN, the upper limits refer to the \( J = 5/2 - 3/2 \) transition. Line flux upper limits reported are at the 3σ level, after spectrospatial filtering. Values in parentheses are upper limits obtained from spatial integration over the region where the continuum is detected at a level \( > 2\sigma \) in each respective data set. References: (1) this work; (2) Matrà et al. (2017a), (3) Dent et al. (2014).
the significance of these upper limits in relation to solar system cometary compositions. We put a special emphasis on the CN/CO ratio upper limit and its consequences for HCN and CO in β Pictoris’ exocometary ices, for reasons that will become apparent in Section 4.2.

4.1. Expanding the Steady-state Cometary Release Model

In order to understand the factors that affect remote detection of molecular species released in the gas phase from exocometary ices, we use the steady-state exocometary gas release model of Matrà et al. (2015, 2017b) and expand it to include molecular species other than CO. Within the framework of this model, the mass production rate $M_i^+$ of molecular species $i$ will equal its destruction rate $\dot{M}_i^-$:

$$M_i^+ = m_i \dot{N}_i^+ = \frac{M_i}{\tau_i}, \quad (1)$$

where $m_i$ is its molecular mass in kg, $\dot{N}_i^+$ its production rate in number of molecules per second, $M_i$ its observed gas mass, and $\tau_i$ its destruction timescale in the gas phase, which we here assume to be dominated by photodissociation, neglecting any other gas-phase chemical reactions ($\tau_i^{\text{phd}} = \tau_i^{\text{phot}}$).

Then, the gas mass of species $i$ we would expect to observe relative to CO is

$$\frac{M_i}{M_{\text{CO}}} = \frac{\tau_i^{\text{phd}}}{\tau_i^{\text{CO}}} \frac{\dot{N}_i^+}{\dot{N}_{\text{CO}}}. \quad (2)$$

If CO and species $i$ are released in the gas at the same rate per molecule (an assumption that we will revisit in Section 5.1), we can directly link an observed gas mass ratio to an ice abundance ratio in the exocomets. Furthermore, this relation shows the crucial impact of the photodissociation timescale on the observable mass of exocometary gas species (see Section 4.2).

The next step is to link the molecular gas mass to line fluxes for given transitions as observed in this work. Following, for example, Equation (2) in Matrà et al. (2015), and assuming optically thin transitions (see Section 5.2), we have

$$\frac{F_{\nu_{i-\nu}}}{F_{\nu_{i-\nu,\text{CO}}}} = \frac{A_{\nu_{i-\nu}}}{A_{\nu_{i-\nu,\text{CO}}}} \frac{x_{A_i}}{x_{A_i,\text{CO}}} \frac{\tau_i^{\text{phd}}}{\tau_i^{\text{CO}}} \frac{\dot{N}_i^+}{\dot{N}_{\text{CO}}}, \quad (3)$$

where, for both CO and species $i$, $F_{\nu_{i-\nu}}$ are integrated line fluxes in Jy km s$^{-1}$, and $A$ and $x_A$ are Einstein $A$ coefficients and upper-level fractional populations of the observed transition. We note that the steady-state relation in Equation (3) remains the same for daughter molecular species such as CN and OH, as long as their production is dominated by a single parent species (such as HCN and H$_2$O).

4.2. The Effect of Photodissociation: Lifetime of Solar System Cometary Molecules

In Figure 3 (left), we present unshielded photodissociation timescales for molecules observed around β Pic as well as other species observed to be abundant in solar system comets. We do not include HCO$^+$ and N$_2$H$^+$ because these ions, if present at all, would likely recombine through free electrons faster than they photodissociate; taking the example of HCO$^+$, using an electron density of $10^2$–$10^3$ cm$^{-3}$ (Matrà et al. 2017a), temperatures between 20 and 100 K, and reaction rates from

the KIDA$^6$ database (Wakelam et al. 2012), we find its recombination timescale is 0.2 to 5 days, much shorter than the $3.7 \times 10^3$ years photodissociation timescale at 85 au from the star.

Photodissociation timescales for all molecules were calculated using photodissociation cross sections from Heays et al. (2017)$^7$ and references therein, neglecting isotope-selective photodissociation for rarer isotopologues. The radiation field includes both the observed spectrum of the β Pic star and the interstellar radiation field (ISRF). The stellar spectrum (A. Branderker 2018, private communication) was obtained by superimposing observed spectra from HST/STIS (Roberge et al. 2000) and the Far-Ultraviolet Spectroscopic Explorer (FUSE; Bouret et al. 2002; Roberge et al. 2006) on the photospheric model spectrum of Fernández et al. (2006). For the ISRF, we adopted the formulation of Draine (1978) with the long-wavelength expansion of van Dishoeck et al. (2006).

We note that the β Pictoris star is surprisingly active for an A-star, with X-ray observations presenting evidence for thermal emission from a cool corona (Hempel et al. 2005; Günther et al. 2012), as well as UV chromospheric emission (Deleuil et al. 2001; Bouret et al. 2002). The latter effectively causes a considerable UV flux “excess” compared to a typical main-sequence A-star; this acts to shorten the survival times of molecules against photodissociation, particularly for molecules whose photodissociation bands lie at shorter UV wavelengths (such as CO; see Figure 3, top right). This leads to a considerable change in the unshielded CO photodissociation timescale for the β Pictoris gas disk; Figure 3 (bottom right) shows that photodissociation at the clump radial location (~85 au) has a significant contribution from the strong UV field of β Pictoris as well as from the ISRF (where the latter would instead dominate for a typical ASV stellar model; Kamp & Bertoldi 2000).

We therefore revise the unshielded CO photodissociation lifetime from 120 years (Kamp & Bertoldi 2000; Dent et al. 2014) down to 42 years. We note that dust shielding is negligible for optically thin dust in debris disks (e.g., Kamp & Bertoldi 2000), and H$_2$O, if at all present, should have a low enough column density not to provide shielding either (Matrà et al. 2017a). CO is, however, abundant enough that self-shielding cannot be neglected (Matrà et al. 2017a). When this is taken into account, the CO lifetime increases from 42 to ~105 years. This is accounted for in all calculations involving CO. We neglect self-shielding and shielding by CO for all other molecules due to their unknown spatial distributions and shielding functions. Neglecting self-shielding should be a good approximation given the much lower predicted abundance of molecules other than CO.

Overall, Figure 3 (left) shows that the harsh UV radiation field around β Pic causes photodestruction of the vast majority of volatile species to take place in timescales of days to months. Therefore, photodissociation alone can explain most of our upper limits, as we confirm more quantitatively in Section 5.2, where we make predictions for future surveys (see Figure 6, right). N$_2$, CO, and CN are by far the longest lasting molecules, having unshielded photodissociation timescales of 96, 42, and 16 years, at least an order of magnitude longer than for any other molecular species. This means that the only observable molecule with a survival timescale similar to that of the

$^6$ http://kida.obs.u-bordeaux1.fr

$^7$ http://home.strw.leidenuniv.nl/~ewine/photo/
detected CO is CN, which we therefore focus on for the rest of this work. In solar system comets, CN gas is produced mainly by photodissociation of HCN gas (Fray et al. 2005); we will here assume that the same applies for exocomets around β Pictoris.

One potential caveat to this assumption is that although for simplicity we have neglected gas-phase chemical production or destruction pathways other than photodissociation, CN could be destroyed by reaction with atomic oxygen O1, which has been detected in the disk around β Pictoris (e.g., Brandeker et al. 2016; Kral et al. 2016). Unfortunately, the detection being unresolved spectrally and spatially combined with excitation and optical depth effects make number-density estimates at the locations where CN is expected to lie very uncertain. Nonetheless, combining a number-density value of $2 \times 10^{7}$ cm$^{-3}$ at 85 au from the best-fit dynamical evolution model of Kral et al. (2016) with a reaction rate of $5 \times 10^{11}$ cm$^{3}$ s$^{-1}$ from the KInetic Database for Astrochemistry (KIDA) database yields a reaction timescale of $\sim$3 years. This is shorter than the CN photodissociation timescale (16 years), indicating that reaction with oxygen could introduce an uncertainty of a factor of a few to our calculations, increasing the inferred HCN/CO outgassing ratio. Given the uncertainty on the oxygen abundance, however, we opt to neglect this destruction pathway of CN in this work.

4.3. The Effect of Molecular Excitation Including Fluorescence

The only unknowns remaining to link the observed $F_{CN,N=2→1,J=5/2→3/2}/F_{CO,J=2→1}$ flux ratio to the $N_{HCN}/N_{CO}$ ratio of the HCN and CO outgassing rates are the fractional populations of the upper levels $x_{N} = 2J + 1 = 5/2$, CN and $x_{J}=2$, CO of the observed line transitions. Matrà et al. (2015) showed that, at least for CO, the assumption of local thermodynamic equilibrium (LTE) is unlikely to apply in the low gas density environments present in debris disks. This prediction was confirmed by CO line ratio observations in β Pictoris (Matrà et al. 2017a) and observations of atomic gas species (Kral et al. 2016, 2017). To determine the CO and CN level populations, we therefore carry out a full nonlocal thermodynamic equilibrium (NLTE) calculation, which includes solving the equations of statistical equilibrium for both molecules. NLTE level populations depend on the local radiation field within the disk, and on the local density of the dominant collider species (here taken to be electrons) $n_{e}$ and the local kinetic temperature $T_{k}$. We direct the reader to Matrà et al. (2015) for details.

Thin dashed and solid lines in Figure 4 show the resulting dependence of the CO and CN upper-level fractional populations $x$ on the electron density and temperature in the gas disk, when applying our previous NLTE model (Matrà et al. 2015). Upper-level populations vary between two limiting regimes, where excitation of the molecules is dominated by either radiation (far left, low $n_{e}$) or collisions (i.e., LTE, far right, high $n_{e}$). As expected, the calculated excitation of the considered CO and CN levels drops by several orders of magnitude in the radiation-dominated regime. This is because the model so far included only low-energy rotational transitions at far-infrared to millimeter wavelengths, which can only be excited by the faint cosmic microwave background and disk continuum emission.
In the Appendix, we expand this NLTE excitation model to include vibrational and electronic as well as rotational levels for both CO and CN. This allows us to account for the effect of fluorescence, which in low-density regimes such as solar system comets and exocometary gas disks, where radiation can dominate excitation, becomes an important excitation mechanism. Fluorescence works through absorption of stellar UV (IR) photons from low rotational levels in the ground electronic and vibrational state to excited electronic (vibrational) levels. This is followed by rapid relaxation to the ground electronic and vibrational state, but to higher rotational levels than the molecule started from. As we can see in Figure 4 (e.g., green versus red lines), this effectively leads to enhanced population of rotational levels above ground, where this can be orders of magnitude higher compared to when fluorescence is not considered. We note that fluorescence matters only in the low-density, radiation-dominated regime (left in Figure 4, thick versus thin lines), whereas populations in the LTE, collision-dominated regime (right in Figure 4) remain unchanged. The extent to which fluorescence impacts molecular excitation depends on the stellar flux received by the molecule and its spectral shape from UV to IR wavelengths.

In general, we find that taking fluorescence into account is crucial when using NLTE excitation models to derive molecular gas masses from observed fluxes. This affects previous CO mass measurements where this effect was not taken into account; while the exact effect depends on the UV and IR flux received by a molecule, which is different for each observed system, the overall effect of the enhanced excitation will be to lower the upper limits in the range of NLTE-derived masses. The total CO mass around β Pic remains largely unchanged as it is tightly constrained observationally through the $J = 3–2 / J = 2–1$ CO line ratio. For completeness, we report an updated value of $3.6^{+0.9}_{−0.6} \times 10^{-5} M_\odot$, calculated in the same way as by Matrà et al. (2017a). Including fluorescence will also lower the electron densities derived in Figure 11 of that work by a factor of a few, bringing them closer to the model predictions of Kral et al. (2016), and flatten their radial distribution in the inner regions of the CO disk.

Taking fluorescence at the clump location into account, we find that the ratio in fractional upper-level populations between CN and CO varies between $0.49$ and $0.71$, with the lowest value for electron densities of $10^{2–10^{3}} \text{ cm}^{-3}$ and temperatures above $50 \text{ K}$. We note that this electron density—temperature dependence of the ratio between CN and CO fractional upper-level populations is much weaker than for each individual upper-level population, due to the similarity in the structure of rotational energy levels between CO and CN.

4.4. Deriving the HCN/(CO+CO$_2$) Ratio of Outgassing Rates

Plugging CN/CO ratios of upper-level populations, photodissociation timescales, and observed fluxes into Equation (3) allows us to derive an upper limit on the HCN/CO ratio of outgassing rates, which will carry the same dependence on electron density and temperature as the ratio between the CN and CO fractional populations mentioned above (colored lines in Figure 4). The lowest CN/CO ratio in upper-level fractional populations sets the most conservative upper limit of 2.5% on the HCN/CO ratio of outgassing rates. An important point to make is that CO gas is also produced via rapid photodissociation of CO$_2$ gas. This implies that if CO$_2$ is being released from cometary ices together with CO, which we deem likely (see discussion in Section 5.1), the CO gas observed has contributions from both the CO and CO$_2$ ice reservoirs. From now on, we therefore consider our upper limit of 2.5% to trace the HCN/(CO+CO$_2$) rather than the HCN/CO ratio of outgassing rates. With this limit, in Section 5 we draw the comparison between β Pictoris and solar system comets, and we discuss the origin of a potential abundance discrepancy.

5. Discussion

5.1. HCN/(CO+CO$_2$) Outgassing Rates in β Pictoris Exocomets versus Solar System Comets

Figure 5 shows our conservative upper limit of 2.5% on the ratio of the HCN/(CO+CO$_2$) outgassing rate in β Pic (red) compared to HCN/(CO+CO$_2$) and HCN/CO values measured in solar system comets from Le Roy et al. (2015) and references therein (orange and blue symbols, respectively). We find that the upper limit we set in β Pic is at the low end of the values derived for comets as they approach the Earth in our own solar system. Although our current upper limit per se does not yet indicate a significant depletion compared to solar system values, we here consider how a low value (and, if confirmed in the future, a true depletion) could be linked to either the outgassing mechanism itself or to the intrinsic HCN/(CO+CO$_2$) abundance in the ice.

The spatial distribution of CO provides an important clue about the gas release mechanism, as CO emission is peaked at a clump located ~85 au from the star (Dent et al. 2014; Matrà et al. 2017a) that coincides with a dust enhancement most clearly observed in mid-infrared imaging (Telesco et al. 2005). This dust enhancement should be associated with higher collisional rates compared to the rest of the belt, and it strongly suggests both the CO and dust enhancements originate from collisions, directly or indirectly.

The measured outgassing rates of molecular species (integrated over all grain sizes) should reflect the ice composition as long as both ice species are released as gas before they reach the bottom size of the collisional cascade (Matrà et al. 2017b). Whether this is the case depends on the details of the release process. Gas may be released during
collisions through at least three mechanisms: (1) direct collisional release of species that should have already sublimated at the temperature characteristic of the belt, but were trapped beneath a layer of refractories or within other ice matrices prior to the collision; (2) thermal sublimation following collisional heating due to, for example, hypervelocity impacts (e.g., Czechowski & Mann 2007); or (3) UV photodesorption of resurfaced ice, which was previously buried below a layer of refractories (Grigorieva et al. 2007).

While CO is considered a supervolatile and is most likely fully lost by the time grains reach the blow-out size (Matrà et al. 2017b), HCN is not and will not sublimate even at the temperature of the smallest grains in the β Pic belt (which dominate the emission and lead to a directly measurable value of ∼86 K from the spectral energy distribution). Such temperature dependence on the relative outgassing rates is observed in solar system comets, where sublimation drives the outgassing and causes the HCN/CO ratio of outgassing rates to decrease with increasing distance from the Sun (Womack et al. 2017). For comparison, we note that β Pictoris is much more luminous than our own Sun ($L_\star = 8.7$ $L_\odot$, Kennedy & Wyatt 2014), and that we are observing exocometary CO at distances of ∼50–220 au, where blackbody temperatures are in the range ∼30–70 K. The same temperatures are attained in the solar system at distances of 19–39 au from the Sun, that is, from the orbit of Uranus out to the Kuiper Belt. This means that β Pic’s exocometes are much colder than observed active comets in our solar system, even compared to the distantly active ones mentioned above (observed at ∼5–11 au from the Sun). This implies that we would expect CO but not HCN to sublimate from β Pic’s exocometes. The question is then whether thermal sublimation is the dominant gas release mechanism in the β Pic disk.

Given the strong UV field from the central A-type star, UV photodesorption of ice resurfaced after collisions is a promising mechanism to release ice species less volatile than CO to the gas phase. The calculations of Grigorieva et al. (2007) show that the timescale for complete UV photodesorption of a pure H$_2$O ice grain is shorter than the collision timescale for grains below ∼20 μm in size. Assuming HCN has a photodesorption yield similar to that of water, and neglecting any trapping within a refractory layer, this implies that all of the HCN ice will be released from grains before reaching the smallest size in the collisional cascade. A similar argument applies to CO$_2$, which has a volatility between that of CO and HCN (Matrà et al. 2017b). UV photodesorption is therefore most likely at play, and if dominant it would imply that HCN and CO$_2$ should be released in the gas phase together with CO, at rates reflecting their ice abundances.

Even if HCN does not photodesorb and survives in the ice phase on the smallest grains in the cascade, it can be thermally sublimated as these unbound grains collide on their way out of the system (Czechowski & Mann 2007). This is because stellar radiation pressure accelerates them to sufficiently high velocities for collisions to provide sufficient heating for sublimation. Application of this model to the β Pic disk shows that this process can release ice (of unspecified composition) in the gas phase (Czechowski & Mann 2007), with gas production rates of the same order as those estimated for CO in the belt. Then, similarly to UV photodesorption, and as long as all ice species are fully sublimated in each impact, high-velocity collisions of unbound grains would also produce gas release rates reflecting ice abundances.

In summary, a low HCN/(CO+CO$_2$) ratio of outgassing rates could be attributed to the gas release mechanism only if this is driven by low-velocity collisions, as this induces release of trapped supervoltiles alone. However, we would expect outgassing of all molecules independent of their sublimation temperatures if UV photodesorption or high-velocity collisions with unbound grains are the dominant outgassing mechanisms. Detailed modeling results (Czechowski & Mann 2007; Grigorieva et al. 2007) show that these processes are most likely at play for small grains in the β Pic belt. Then, unless most CO is being released through low-velocity noncatastrophic collisions between large bodies at the top of the cascade (which are not taken into account by our model; see Matrà et al. 2017b), we would expect ratios of outgassing rates to reflect cometary ice abundances. These can then be directly compared with relative abundances from solar system comets, measured as they come close enough to the Sun for their ratios of outgassing rates to reflect ice compositions.

In the scenario where outgassing in the β Pic belt is dominated by UV photodesorption or high-velocity collisions of small grains, our upper limit on the HCN/(CO+CO$_2$) ratio of outgassing rates for β Pic’s exocometes suggests an HCN/(CO+CO$_2$) ice abundance ratio that is at the low end of the range observed in solar system comets, although still not exceptionally low. Future, deeper observations (Section 5.2) are required to conclusively determine whether the abundance of β Pic’s exocometes is truly abnormal compared to solar system comets.
Determining the abundance of HCN in exocomets is especially interesting because of its connections to the origins of life chemistry (e.g., Powner et al. 2009). The large scatter in HCN abundances observed among solar system comets (Mumma & Charnley 2011, and references therein) and observation of cyanides in protoplanetary disks (Öberg et al. 2015; Guzmán et al. 2017; Huang et al. 2017) indicate that cometary cyanides may not be directly inherited from the ISM, but undergo active chemical processing during the epoch of planet formation. Whether the endpoint of this chemistry is different for different planetary systems is yet unclear and can only be resolved by future, deeper observations of exocometary cyanides.

5.2. Predictions for Molecular Surveys of Gas-bearing Debris Disks

To guide future observations, we use Equation (3) to calculate predicted line flux ratios around β Pictoris for all common cometary species, taking into account the range of abundances observed in the solar system. We make two main assumptions. First, we assume all species are collocated with CO, leading to similar spatial distributions and excitation conditions. Since the bulk of the CO emission originates from the SW clump at 85 au from the star, we use the stellar radiation field at 85 au as representative of the bulk of the gas disk. Second, we calculate the excitation of all species using the LTE approximation (apart from CO itself, where the level populations are very well constrained by the existing J = 3–2/ J = 2–1 line ratio; Matrà et al. 2017a). Figure 4 shows that the LTE assumption does not affect the calculated populations of CN and CO by more than a factor of a few for low energy levels, but we cannot exclude that this may have a significant effect for other molecules and higher transitions. We vary the gas kinetic temperature between 52 K (as predicted by thermodynamical models at the clump location; Kral et al. 2016) and 210 K (as the upper limit estimated through the resolved CO scale height at the clump location; Matrà et al. 2017a).

We focus on molecular transitions observable with currently available facilities at far-infrared to radio wavelengths, namely the Stratospheric Observatory for Infrared Astronomy (SOFIA), ALMA, and the Karl G. Jansky Very Large Array (VLA). We select the best observable transition for each temperature and molecule to be that with the highest “effective S/N.” We construct this by dividing a transition’s flux ratio with respect to CO (as calculated above) by the sensitivity of each telescope facility considered, at the frequency of the given transition. In addition, we consider the telescope’s resolution by dividing this effective S/N by \( \sqrt{N_{\text{beams}}} \), where \( N_{\text{beams}} \) is the number of resolution elements covering the gas disk. As this acts to penalize facilities that overresolve the gas disk, we choose a resolution closest to the CO disk’s on-sky diameter (\( \sim 16''/5 \); Matrà et al. 2017a) for the ALMA and VLA interferometers. This is a conservative approach as the spectral stacking technique described in Section 3.2 (Matrà et al. 2015) should significantly alleviate the sensitivity loss caused by overresolving the disk.

Having selected the best transition for each molecule and temperature, we show its range of fluxes expected for solar system cometary abundances in Figure 6, left (vertical bars). We only show predictions for a single temperature of 52 K, as we find that the maximum effective S/N achievable for most species is largely independent of temperature (since, e.g., for higher temperatures, higher transitions will emit more strongly and can then be selected for observations). These predictions can then be compared with each telescope’s 3σ detection thresholds (green bars), where these also take into account that the disk will be resolved (darker as opposed to lighter bars for unresolved emission). We find CN (as expected) but also HCN and OH to be promising molecules for detection around β Pic. This is largely due to their transitions having Einstein A coefficients orders of magnitude larger than CO, compensating for their lower gas masses caused by their shorter photodissociation timescales.

Since the predicted line fluxes can, in a few cases, be up to orders of magnitude higher than CO, we need to consider that these transitions may be optically thick, particularly since CO itself has modest optical depth at the clump location (\( \tau_{\text{CO}} = 2.1 \sim 0.12 \)). To estimate optical depth, we first take the CO column density at the clump location as determined through \( J = 3–2/J = 2–1 \) line ratio observations (Matrà et al. 2017a). Then, we scale this by the abundance ratio of molecule i with respect to CO in the gas, to find the column density of molecule i. This can be combined with LTE fractional populations to solve for the optical depth through its definition (Equation (3), Matrà et al. 2017a), scaling the velocity width of the line to the Doppler-broadened width of the molecule in question. We find that the predictions, when accounting for optical depth effects (solid as opposed to dotted vertical bars in Figure 6), change significantly only for the OH \(^2\text{H}_2/ J = 5/2^–/3/2^– \) line at 2.51 THz.

Overall, if cometary volatiles are being released at rates reflecting their ice composition, and if their composition reflects that of solar system comets, we expect CN and HCN to be readily detectable with ALMA around β Pictoris. Given that CN photodissociation takes place through photons of a wavelength similar to those causing CO photodissociation, we expect the CN/CO flux prediction to hold for exocometary gas disks around different stars as well.

An interesting result of our calculation is that OH detection should be possible with SOFIA. This encouraged us to check the Herschel Science Archive, where we found unpublished PACS observations of β Pictoris covering the OH line. We extracted the point-source-corrected spectrum from the central 7″ spaxel of the PACS Level 3 data product and scaled it to the total flux of the central 3 × 3 spaxels. Then, we carried out continuum subtraction through a second-order polynomial, leading to a measured rms noise level of 0.24 Jy. Given the coarse spectral resolution of the data (295.2 km s\(^{-1}\) at 119.3 μm), we assume the line is unresolved to set a 3σ upper limit on the integrated line flux of 2.1 × 10\(^5\) Jy km s\(^{-1}\). We find that this is already at the very low end of our predicted range. However, given the significant optical thickness of the line, our prediction is very sensitive to the choice of OH temperature or spatial distribution, which may be oversimplified here.

We find detection of rotational lines from the \(^1\)H\(^2\)O water isotopologue, hydrogen sulfide (H\(_2\)S), and ammonia (NH\(_3\)) to be very unlikely with current instrument capabilities, although ammonia may be detectable in the future with the sensitivity improvement brought by the Next Generation Very Large Array.\(^9\) On the other hand, we can already probe solar system

\(^8\) Herschel Observation ID: 1342198170.
\(^9\) http://library.nrao.edu/public/memos/ngvla/NGVLA_17.pdf
6. Conclusions

We have presented the first molecular survey of the exocometary gas disk around β Pictoris with the SMA, and we combined it with archival ALMA data to obtain coverage of 10 different molecular species, namely CO, CN, HCN, HCO+, N$_2$H$^+$, H$_2$CO, H$_2$S, CH$_3$OH, SiO, and DCN. We reported continuum and CO $J = 2$–1 detections and used upper limits on all other species as the basis to expand an exocometary release model beyond CO. We obtain the following conclusions:

1. The (optically thin) line fluxes for a given molecule depend on its exocometary outgassing rate, its photodissociation lifetime (neglecting other gas-phase chemical reactions), its intrinsic line strength, and the fractional population of the upper level of the transition (Equation (3)). Knowledge of this upper-level population requires NLTE excitation modeling, which we here expand to include the effect of fluorescence. We find that the latter produces orders of magnitude higher excitation in the low gas density, NLTE regime and needs to be taken into account for robust derivation of gas masses from observed line fluxes.

2. CO is the longest lived cometary molecule against photodissociation that is observable at millimeter wavelengths. This long lifetime explains, in part, why it is the only one that has been detected so far. Other observable molecules have survival lifetimes several orders of magnitude below that of CO, except for CN. This makes CN the most promising molecule for detection in debris disks after CO.

3. CN is a daughter molecule, which we assumed to be produced mostly through photodissociation of HCN gas released from the ice phase. CO gas, on the other hand, is both a parent and daughter species produced by CO$_2$ photodissociation. Therefore, we used our upper limit on the CN/CO flux ratio to derive an upper limit on the HCN/(CO+CO$_2$) ratio of outgassing rates of 2.5%. This is still consistent with, although below, most of the values measured in solar system comets as observed near Earth. If deeper CN or HCN observations push this HCN/(CO+CO$_2$) outgassing rate upper limit down to a significant depletion compared to solar system comets, we show that this may be caused by either the outgassing mechanism or a true depletion in the ice abundance.

4. Outgassing ratios of molecular species reflect their ice compositions as long as ices cannot survive on grains down to the blow-out size in the collisional cascade and be removed from the system. This is likely the case in β Pictoris, as (1) collisions will allow ice layers to resurface, where they become subject to rapid UV...
photodesorption (Grigorieva et al. 2007), and (2) the smallest unbound grains will undergo hypervelocity collisions on their way out of the system, leading to vaporization of any ice that may have survived on these grains (Czechowski & Mann 2007). In general, these processes will allow release of molecules less volatile than CO that would otherwise survive in the ice phase on the smallest grains and be dynamically removed by radiation pressure from the central star.

5. Then, unless noncatastrophic collisions at the top of the cascade are the dominant gas release mechanism, a low HCN/(CO+CO2) outgassing rate is attributed to a low HCN/(CO+CO2) abundance in the exocometary ice. If confirmed by deeper observations, this would indicate that active cyanide chemistry during planet formation produces a wide variety of cometary compositions across planetary systems.

6. We present predictions for future detection of cometary species around β Pictoris, assuming solar system abundances and LTE excitation. We find that ALMA should readily detect CN and HCN line emission, even for the most HCN-poor solar system abundances. Other species such as H2O, HDO, H2CO, CH3OH, and DCN may be detectable, depending on their specific composition, spatial distribution, and excitation conditions.

7. Finally, we report Herschel archival upper limits on the OH 2Π1/2 J = 5/2− 3/2− line at 2.51 THz that are already at the very low end of the range predicted assuming LTE and solar system cometary H2O abundances. The line is optically thick, and hence the flux prediction is sensitive to the assumed on-sky distribution and temperature of OH gas, which are likely oversimplified here. Further modeling taking these effects into account is needed to evaluate whether this upper limit indicates an underabundance of water in β Pic’s exocometes, and whether SOFIA may be able to detect OH from photodesstruction of water in exocometary gas disks.

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Facilities: SMA, ALMA, Herschel.

Software: MIR, miriad (Sault et al. 1995), CASA (McMullin et al. 2007), Matplotlib (Hunter 2007).

Appendix

Solving the Statistical Equilibrium for CO and CN Including Fluorescence

We direct the reader to Section 2 in Matrà et al. (2015) for a detailed explanation of how to calculate the rotational excitation of a molecule (using the example of CO) for a given radiation field J, density of collisional partners n_{coll}, and kinetic temperature T_{kin}. In summary, the total rate of radiative and collisional transitions populating each of the N_{lev} energy levels is equated to the total rate of transitions depopulating the level. The statistical equilibrium calculation involves solving this system of N_{lev} linear equations to obtain the fractional population x of each energy level (defined as the number of molecules in that level divided by the total number of molecules).

We here expand this calculation to include not only rotational transitions (lowest energy, corresponding to far-IR/mm wavelengths) but also vibrational (near/mid-IR) and electronic (UV/optical) transitions. This inclusion is important in the presence of strong UV/IR radiation fields such as in our case of optically thin gas around an early-type star. Although in this work we are only interested in the population of rotational levels, as it affects our observed millimeter lines, absorption of UV photons is important as well. The latter can excite the molecule to high electronic states followed by rapid relaxation to the ground electronic state. However, this relaxation takes place via cascading through excited vibrational or rotational states (i.e., fluorescence), and this may significantly affect the rotational populations we are interested in (see Figure 1 in Thi et al. 2013 for a schematic view of the process for the CO molecule).

For CO, we obtain radiative transition rates from Thi et al. (2013) and references therein. For CN, pure rotational radiative rates were obtained from Klish et al. (1995) using the dipole moment of Thomson & Daly (1968) through the LAMDA database (Schöier et al. 2005), whereas all other rovibrational/electronic radiative rates were obtained from Brooke et al. (2014) through the ExoMol database (Tennyson & Yurchenko 2012). This resulted in our compilation of all allowed radiative transitions between any of the two (three) lowest electronic levels, nine (six) lowest vibrational levels, and 30 (20) lowest rotational levels for CO (CN). For CN, each rotational level (N) apart from N = 0 is divided into two closely spaced fine-structure (J) levels for all electronic and vibrational levels; in addition, J levels in the A−Π state (first electronic state above ground) are further subdivided into two levels due to Λ-doubling. We neglect hyperfine splitting of the lines, which acts to create subtransitions that are mostly blended within the Keplerian velocity structure of each fine-structure (J) transition observed.

The gas kinetic temperatures in gas-bearing debris disks are expected to be on the order of a few tens of kelvins, as predicted by thermodynamical models (Kral et al. 2016) and as suggested by the CO excitation temperatures observed so far (e.g., Hughes et al. 2017; Matrà et al. 2017a). This means that the collisional population of excited vibrational and electronic energy levels (corresponding to temperatures of thousands to
tens of thousands of kelvins, respectively) can be neglected. Therefore, we only include collisional transitions between the rotational levels of the ground vibrational and electronic state, using rates from Dickinson & Richards (1975) for CO and from Allison & Dalgarno (1971) through the LAMDA database for CN.

Calculating the absorption and stimulated emission rates between any two levels of the molecule requires knowledge of the radiation field \( J \) at a frequency \( \nu \) corresponding to the energy difference between the two levels. Given the inclusion of UV and near-infrared as well as millimeter transitions, knowledge of the radiation field from UV to millimeter wavelengths as felt by a molecule at a given location in the gas disk is required. We take into account contributions from the cosmic microwave background (CMB), the star (using the same spectrum as in Section 4.2), and the disk’s dust continuum emission. For the latter, we use the best-fit 3D model to ALMA millimeter continuum observations (L. Matrà et al. 2018, in preparation) to measure the radiation field within the disk itself, as described in Appendix B of Kral et al. (2017); we then scale the total disk emission to other wavelengths using unresolved spectral energy distribution flux measurements. However, we find inclusion of the dust continuum radiation field to have a negligible effect on the excitation calculation. This is because the dust continuum is sufficiently faint that absorption of stellar UV photons and subsequent spontaneous emission take place on a shorter timescale than absorption and stimulated emission from IR dust continuum photons. In addition, the CMB dominates excitation over the dust continuum for the low-lying rotational transition of interest here (as found for Fomalhaut in Matrà et al. 2015, Figure 3).

Figure 7 shows the results of the statistical equilibrium calculation for the pure rotational ladder (ground vibrational and electronic state), which is relevant to millimeter observations such as described in this work. In particular, the fractional populations \( x \) of levels \( N = 2, J = 5/2 \) for CN and \( J = 2 \) for CO (highlighted by the orange line) are the ones displayed in Figure 4 as a function of the kinetic temperature and electron density of the gas. From that figure, it is clear that for each level, two limiting regimes are present (in line with our expectation; see, e.g., Matrà et al. 2015); in the very low gas density regime (which we here call “far-NLTE”), excitation by radiation dominates, whereas in the high gas density regime it is collisional excitation that dominates (LTE). In both limiting regimes, the excitation becomes independent of the gas density; in the radiation-dominated regime, the excitation is also independent of temperature, whereas in LTE it is independent of the impinging radiation field.

In the bottom (upper) panel of Figure 7, we show how the rotational populations up to level \( J = 10 \) \((N = 10)\) for CO (CN) behave in each limiting regime (LTE or far-NLTE). We vary the temperature (affecting the LTE limit) and the distance from the star (affecting the stellar flux and hence the fluorescence mechanism in the NLTE limit). We also compare the NLTE results where fluorescence is turned on or off. As expected, in LTE (+ symbols), higher levels are preferentially populated at higher temperature, and our statistical equilibrium results match the analytical calculation from the Boltzmann distribution. In NLTE, we find that turning on the stellar UV field and hence the fluorescence mechanism (solid circles) leads to a significant population of rotational levels above ground compared to the case where fluorescence is not considered (red triangles). As we would expect, high rotational levels are even more favored compared to low levels as we move closer to the star and thus increase the effect of fluorescence.

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![Figure 7](https://example.com/figure7.png)
