Metamorphic Testing and Debugging of Tax Preparation Software

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Abstract—This paper presents a data-driven debugging framework to improve the trustworthiness of US tax preparation software systems. Given the legal implications of bugs in such software on its users, ensuring compliance and trustworthiness of tax preparation software is of paramount importance. The key barriers in developing debugging aids for tax preparation systems are the unavailability of explicit specifications and the difficulty of obtaining oracles. We posit that, since the US tax law adheres to the legal doctrine of precedent, the specifications about the outcome of tax preparation software for an individual taxpayer must be viewed in comparison with individuals that are deemed similar. Consequently, these specifications are naturally available as properties on the software requiring similar inputs provide similar outputs. Inspired by the metamorphic testing paradigm, we dub these relations metamorphic relations as they relate to structurally modified inputs.

In collaboration with legal and tax experts, we explicaded metamorphic relations for a set of challenging properties from various US Internal Revenue Services (IRS) publications including Form 1040 (U.S. Individual Income Tax Return), Publication 596 (Earned Income Tax Credit), Schedule 8812 (Qualifying Children and Other Dependents), and Form 8863 (Education Credits). While we focus on an open-source tax preparation software for our case study, the proposed framework can be readily extended to other commercial software. We develop a randomized test-case generation strategy to systematically validate the correctness of tax preparation software guided by metamorphic relations. We further aid this test-case generation by visually explaining the behavior of software on suspicious instances using easy-to-interpret decision-tree models. Our tool uncovered several accountability bugs such as non-robust behavior in corner-cases (unreliable behavior when tax returns are close to zero) to missing eligibility conditions in the updated versions of software.

I. GENERAL ABSTRACT

The authors present a framework for supporting software developers and regulators in testing and auditing sociolegal critical software systems. The key barriers to the automation of the analysis for such software include: 1) the unavailability of correctness requirements and 2) the difficulty of obtaining ground truths for program inputs. The authors posit that, since the US legal system adheres to stare decisis (to stand by things decided) doctrine, the specifications about the outcome of legal-critical software for an individual must be viewed in comparison with individuals that are deemed similar. Such specifications are dubbed metamorphic relations in this work due to their semblance with metamorphic testing paradigm from software engineering. The paper proposes a specification language to express metamorphic relations and uses it to automate the search for suspicious or incorrect behavior of a given software system and uses machine learning algorithms to present a succinct explanation of the identified vulnerabilities.

As a paradigmatic example of sociolegal critical software, the paper focuses on an open-source implementation of the US tax preparation software. The authors explicad metamorphic relations for a set of challenging properties from various US Internal Revenue Services (IRS) publications including Form 1040 (U.S. Individual Income Tax Return), Publication 596 (Earned Income Credit), Schedule 8812 (Qualifying Children and Other Dependents), and Form 8863 (Education Credits). The framework is demonstrated to be useful in uncovering several accountability bugs such as non-robust behavior in corner-cases and missing eligibility conditions.

II. INTRODUCTION

The ever-increasing complexity of income tax laws in the United States has rendered manual preparation of tax returns cumbersome and error-prone. According to the IRS, 90 percent of tax filers filed taxes electronically in 2020 [1]. Consequently, US tax preparation has grown into a $11.2bn industry requiring the services of professional tax accountants or commercial tax preparation software. The use of software is increasing, and in 2020, over 72 million people prepared their taxes without the help of tax professionals, a 24 percent increase from 2019 [2].

Even though there are some freely available open-source alternatives [3], [4], [5], such tax preparation software and services are provided on “AS-IS” bases and may not go through rigorous software development process. The impact of bugs in software are aggravated by the fact that, in the US
tax courts, individuals are accountable for any errors resulting from software bugs in such packages:

**Langley v. Comm’n, T.C. Memo. 2013-22.** The misuse of tax preparation software, even if unintentional or accidental, is no defense to accuracy-related penalties under section 6662.

However, users might not be aware of errors in the software. And few checks currently exist to ensure the correctness of tax software [6]. To protect consumers in this process, we develop validation and debugging aids for open-source tax preparation software. Particularly because this problem has the potential to compound financial stresses of the lower income earners, who are more likely to use freely available and unregulated software [6].

This paper presents a data-driven debugging framework to discover and explain bugs in tax preparation software systems. There are three concrete obstacles to this framework.

- **Absence of Oracle.** The class of correctness requirements for tax preparation systems are not explicitly available since the correct tax-filing is highly subjective to individual taxpayers (this is known as oracle problem [7]).
- **Lack of trustworthy dataset.** While, in the absence of such explicit specification, one can recourse to data-driven approaches, it is difficult to obtain access to a valid dataset due to obvious privacy and legal concerns.
- **Computational infeasibility.** Even when one can justify fabricating such a dataset, the final challenge is computational in nature: detecting and explaining the bug by comparing an individual decision to others over a large dataset based on a given similarity measure is computationally intractable.

Metamorphic testing [8] is a software testing paradigm that tackles the oracle problem by considering software properties where the correctness of the software on an input does not require knowing the “ground truth” for that input; rather, the correctness can be validated by comparing the output of software for that input with the output of a slightly metamorphosed one. For instance, consider a program implementing a search engine: while there is no way to verify that the results returned for a particular keyword are correct (oracle problem), it is reasonable to expect that a correct search engine should return fewer results for a more restricted keyword.

This paper makes a case for the suitability of metamorphic specifications in testing and debugging tax preparation software (and by extension for legal software systems). We address aforementioned challenges by integrating metamorphic specifications with data-driven debugging in the following manner:

- **Metamorphic Specifications.** The first obstacle in developing the debugging framework is to explicate an appropriate notion of correctness requirements. Note that, given the relevant information about an individual, resolving the correct decision for that individual requires accounting and legal expertise. Hence, obtaining the oracle for testing and debugging purposes is impractically expensive. Fortuitously, since the US tax law is a law code, it adheres to principle of common law and implements stare decisis, i.e., the legal doctrine of precedent: similar cases must follow similar rulings. As a corollary, the correctness of tax preparation software must also be viewed in comparison with similar cases. In other words, the correctness properties can be expressed as relations (1) between two individual taxpayers with similar situations, i.e., a notion of horizontal equity in taxation [9] and (2) between two taxpayers in different tax income buckets, i.e., a notion of vertical equity in taxation [10]. Following the metamorphic testing [8], we call such properties metamorphic specifications. In collaboration with tax experts, we reviewed some critical correctness properties of tax preparation outcomes and observed that they are naturally expressible as metamorphic specifications. One key contribution of this paper is to explicate formal representations of these properties from the latest Internal Revenue System (IRS) documents.

- **Test-case Generation.** While it is an arduous task to compare an individual situation with the precedents, the availability of software artifacts implementing the tax laws permit us to query the tax outcomes for fictitious individuals similar to a given individual. This combined with the metamorphic nature of the requirements allows us validate the software system by comparing the results for a given (source) individual with its (metamorphosed) follow-ups. We develop a random search strategy to sample source and follow-up test cases from the metamorphic relations and label them as passed or failed.

- **Data-Driven Debugging.** Given a set of test cases with ‘pass’ or ‘fail’ labels over a metamorphic relation, decision trees, as a white-box ML model, are a natural choice to discriminate between the classes and synthesize circumstances under which the software fails [11], [12].

The proposed framework is implemented as the tool TENVFORTY (named after the US individual tax return form 1040). We performed experiments on OpenTaxSolver [3] (tax years of 2018-2021), a popular open-source tax preparation software [13], [14], in five aspects of disability, credits, and deductions that are known to be challenging and error-prone [15]. In particular, we explicated 16 metamorphic relations for the tax year of 2020 in those areas and with little effort, we managed to adapt them for the other tax years (2018, 2019, and 2021). We use these relations to generate test cases as well as oracles. Specifically, our technique generates tens of thousands of random test cases using the metamorphic properties. We explain the circumstances under which the software has both failed and passed cases using CART decision tree algorithm [16]. We provide debugging supports in both spaces of input variables (fields/items in the tax preparation software) and internal variables (conditions, loops, and function calls). As a result, TENVFORTY revealed three types of failures in OpenTaxSolver: missing some eligibility conditions (e.g., married people filing separately status is not eligible to take earned income credits); software fails to satisfy the correctness requirements when
the computed tax returns get very close to zero (small non-zero values); and the updated software that allows users to explicitly opt for an option does not satisfy some correctness requirements in the corner cases.

III. BACKGROUND

The US tax code is based on over 2,600 pages of legal statutes from congress. These statutes are accompanied by IRS regulations, rulings, and clarifications, together amounting to nearly 9,000 pages. Lawsky et al. [17, 18] have extensively studied the structure of the US tax code and have made a convincing case for the need of formal legal reasoning. The structure has gone so complex that the IRS publishes updated instructional resources every fiscal year. Lawsky attributes part of the complexity of US tax codes to internal dependencies, referring to the interlinked nature of calculations across sections of tax forms [17]. This is evident as 97% of references in the Internal Revenue Code (IRC) are internal. Internal dependencies can lead to legal avoidance, when the tax code is not adhered to as intended [18] and can occur when the IRC is misinterpreted. At this point, there has been limited effort to test U.S. tax software that attempts to prepare tax filings in a manner consistent with the extensive tax code.

A study by Nina E. Olson (National Taxpayer Advocate), published by IRS [19], analyzed several (free) tax filing software for the tax year of 2005. The study designed four fictitious scenarios, including some in which the taxpayer qualified for special tax benefits enacted to help Hurricane Katrina victims (See [19, p.11-p.19]). The study found that several of the software did not prompt the taxpayers about these provisions. Therefore, taxpayers ended up not getting the benefits designed for them. Despite being hypothetical, the approach uncovered flaws in the tax filing software and underscored the need for trustworthiness besides software privacy and security. Our approach seeks to automate such discoveries in tax preparation software and provide intuitive explanations.

The absence of logical specifications and oracle in the context of tax preparation software, led us to investigate metamorphic testing. Metamorphic testing [8] is primarily developed to counter the lack of oracle [7] (black box module to decide whether the output of the system is correct for a given input). The idea behind metamorphic testing is to establish correctness by reasoning about relations between multiple input-output behaviors [20]. One example is to validate search engines. While we do not know the ground truth number of return items for any search query $x$, we can expect that for any query $x_1 = x$ and its restrictive one $x_2 = x + k$ with more keywords, the number of retrieved items for $x_1$ is greater than $x_2$. For another example, consider a program that implements $\sin(x)$ function. While we do not know the exact outcome of function for an arbitrary $x$, we can establish that for any $x_1$ and its metamorphosed $x_2 = 2\pi + x_1$, $\sin(x_1) = \sin(x_2)$. In this example, $x_1$ is a source (base) test, and $x_2$ is a follow-up (metamorphosed) test constructed by transforming the source to satisfy the metamorphic relation between $x_1$ and $x_2$ and check the equality between outcomes.

Metamorphic properties have been successfully used to validate a variety of software systems. They have been adapted to validate machine learning classifiers [21], autonomous vehicles [22], Google/Yahoo search engine [23], and social media apps like Facebook [24]. To the best of our knowledge, this work is the first to adapt metamorphic relations in tax preparation software domain as a sociotechnological system.

IV. OVERVIEW

As a demonstration of our framework (shown in Figure 1), this section describes how we tested OpenTaxSolver [3] (versions for the tax years 2018-2021) in one of 5 domains considered in this paper: the Earned Income Tax Credit (EITC). The earned income tax credit is designed to lower the tax burden for low and moderate income workers.

Extract Scenarios. The first step involves carefully examining the rules and regulations. For the EITC, we extract scenarios from Worksheet 1 in Publication 596 [25].

Metamorphic properties. We specify 4 metamorphic relations for EITC, as shown in Table I with EITC (3)-(6) for the tax year 2020, and update these properties for the tax years 2018, 2019, and 2021 as shown in Table II. Property #3 specifies that married filing separately (MFS) is not eligible to take EITC credits in the tax year 2020, noting that the same condition applies for the tax years 2018 and 2019, but the requirement has changed for the tax year 2021 where MFS status is eligible to take the EITC credits (see Table II). Property #4 describes that individuals who are married filing jointly (MFJ) are eligible if their adjusted gross income (AGI) is below or equal to 56,844 for the tax year 2020. Note that different years have different thresholds of eligibility as shown in Table II. Property #5 says that an eligible individual with EITC claim (Line 27 of IRS 1040) should receive equal or higher tax returns compared to metamorphosed individuals who are not eligible due to their AGI, conditions on their dependents, or zero claims of EITC. Finally, property #6 establishes that among two similarly eligible individuals, the one with the higher EITC claims should receive a higher tax return. Other metamorphic relations are described and formulated in Section VII-RQ1.

Random Test-Case Generations. We generate test cases from these metamorphic properties. We encode each metamorphic property as a search problem where the objective is to find an individual and its metamorphosed one such that their deviations from expected outcomes are maximum. We sample data points uniformly at random to generate the source test case and perturb it to generate follow-ups from its neighbors. We sketch the detail of search algorithm to generate test cases in Algorithm 1. The results of experiments for generating test-cases are shown in Table III. Within 15 minutes of search, our implementation of the algorithm in TENFORTY generate over 19k, 18k, 36k, and 36k, for properties #3 to #6, respectively, for the 2020 version (see Table III for the complete experimental results).
The results show that the software fails for some or all test cases of properties #3-#4 in the version 2020, but passes for all test cases of these two properties in the versions 2018 and 2019. While, the 2021 version of software fails for property #3, it passes all test cases for property #4. We found that the updated tax policy where the MFS status is eligible for EITC in 2021 leads to the expected behavior of software for property #4 without explicit modifications compared to the faulty 2020 version! The details of experiments for test-case generations can be found in Section VII-RQ2.

**Explaning Failure Circumstances.** Given the set of passed and failed inputs, we use a decision tree algorithm (detailed in Section VI) to infer conditions under which software fails to satisfy the metamorphic relations. Since the software satisfies the metamorphic relations, the premise of the metamorphic relation itself simply explain the failure circumstances: the tax software does not appropriately check eligibility on the basis of AGI1st row). It shows that the software satisfies the metamorphic relation when AGI is below $16,720 and the federal tax return is below $80. This might be expected due to eligibility for some credits when the tax returns are very low. The decision tree artifacts for other properties are also shown in Table IV. Beyond EITC, the decision trees show that software might fail due to the numerical approximation for small non-zero values and missing to consider all conditions when updated to allow to opt for an option. The experiments for debugging are provided in Section VII-RQ3.

**V. PROBLEM STATEMENT**

The functional model of tax software consists of a tuple $(X, \mathcal{F})$ where $X = \{X_1, X_2, \ldots, X_n\}$ is the set of variables corresponding to various fields about an individual in the tax return form and $\mathcal{F} : D_1 \times D_2 \times \cdots \times D_n \rightarrow \mathbb{R}_{>0}$ is the federal tax return computed by the software, where $D_i$ is the domain of variable $X_i$. We write $\mathcal{D}$ for $D_1 \times D_2 \times \cdots \times D_n$.

These variables correspond to intuitive labels such as age (numerical variable), b1ind (Boolean variable), and gtsa (filing status with values such as MFJ, married filing jointly, and MFS, married filing separately). For an individual $x \in \mathcal{D}$, we write $x(i)$ for the value of $i$-th variable, or $x.1$ for the value of variable $1$ab. Let $\mathcal{L}$ be the set of all labels.

For labels $L \subseteq \mathcal{L}$ and inputs $x \in \mathcal{D}$ and $y \in \mathcal{D}$, we say that $y$ is a metamorphose of $x$ with the exceptions of labels $L$, and we write $x \equiv_L y$ if $\forall \ell \not\in L$ we have that $x.\ell = y.\ell$. A metamorphic relation is a first-order logic formula with variables in $X$, constants from domains in $\mathcal{D}$, relation $\equiv_L$, comparisons $\{<, \leq, >, \geq\}$ over numeric variables, predicate $\neg$ (negation) for Boolean valued labels, real-valued function for federal tax return $\mathcal{F} : \mathcal{D} \rightarrow \mathbb{R}$, Boolean connectives $\land, \lor, \not\land, \not\lor$, and quantifiers $\exists x.\phi(x)$ and $\forall x.\phi(x)$ with natural interpretations. For instance, we assume that the formulas are given in the prefix normal form, i.e. a block of quantifiers followed by a quantifier free formula. Using metamorphic relations, we can express the property

$$\forall x, y (x \equiv_{age} y \land (x.age \geq y.age) \implies (\mathcal{F}(x) \geq \mathcal{F}(y))).$$

**Falsification Problem.** Given a tax preparation software $(X, \mathcal{F})$ and a metamorphic property $\phi$, the falsification problem is to explore the input space of the software to discover inputs that falsify the property. Metamorphic properties containing only one variable are classical properties relating inputs to outputs; however for properties with more than one quantified variables, multiple inputs are required to evaluate the property. Observe that the metamorphic property falsification problem is PSPACE-hard as it is expressive enough to encode True Quantified Boolean formula (TQBF) problem (when the input variables are Boolean and program logic encode Boolean constraints). Hence, it is intractable to provide an exhaustive search procedure. To overcome this challenge, we propose randomized search-based testing approach.

Depending upon the number and nature of of quantifiers, multiple inputs need to be sampled to ascertain the status of the property. Moreover, when the input space is large or infinite, we may not be able to falsify subformulas of the form $\exists x.\phi(x)$ as it would require testing the whole state space. To overcome this challenge in practice, we recoursce to statistical testing guided by randomized exploration of the state space. In the next section, we present a sampling strategy to falsify properties of the form $\forall x.\phi(x)$; this procedure can be recursively invoked to provide the procedure for metamorphic properties with arbitrary quantification.
Algorithm 1: RANDOMTESTCASEGENERATION

Input: Tax preparation software \( \mathcal{P} \), initial input seeds \( I \), metamorphic property \( \mathcal{P} \), a tolerance threshold \( \delta \), a Bayes factor \( B \), a lower-bound on the confidence \( \theta \), and timeout \( T \).

Output: Passed/Failed, test cases, decision tree

\[
(x_m, \Delta_{\text{FTR}}, \text{res}) \leftarrow \text{SAMPLE}(I, 0, \text{True})
\]

while \( \text{time()} - \text{start\_time} < T \) do

\[
k \leftarrow 0
\]

\[
x_1 \leftarrow \text{UNIFORMPERTURB}(x_m, p)
\]

\[
x_2 \leftarrow \text{UNIFORMPERTURB}(x_1, p)
\]

\[
\Delta \leftarrow \text{DISTANCE}(\mathcal{P}(x_1), \mathcal{P}(x_2))
\]

if \( \Delta > \delta \) then

\[
I.\text{ADD}((x_1,x_2);'\text{failed}')
\]

if \( \Delta > \Delta_{\text{FTR}} \) then

\[
x_m \leftarrow x_1
\]

\[
\Delta \leftarrow \Delta_{\text{FTR}}
\]

\[
\text{res} \leftarrow \text{False}
\]

else

\[
I.\text{ADD}((x_1,x_2);'\text{passed}')
\]

\[
k \leftarrow k + 1
\]

if \( k < \frac{\log B}{\log \theta} \) then

\[
\text{Go to 5}
\]

if \( I['\text{passed}'] = \{\} \lor I['\text{failed}'] = \{\} \) then

\[
\text{return } p
\]

else

\[
I' \leftarrow \text{FEATUREENGINEERING}(I)
\]

\[
t \leftarrow \text{DTCCLASSIFIER}(I')
\]

\[
\text{return res, } I, t.
\]

VI. APPROACH

We develop an efficient metamorphic testing and debugging to uncover bugs in tax preparation software. Algorithm 1 sketches different steps in our approach. We start from some initial seed inputs \( I \). In each step, the search strategy selects and perturbs inputs from the set of promising inputs (those maximizing the deviant from the expected outcome) and generates a base test case (line 4). Then, it perturbs the base to generate follow-up cases (line 5). Next, it executes the base and follow-up inputs on the target software and quantifies the deviant between the outcomes (line 6). If the deviant is more than a threshold, it adds the inputs with ‘failed’ label (line 8). Furthermore, if the deviant is higher than any previous ones, it adds the inputs as promising ones (line 9). Otherwise, it adds the inputs with ‘passed’ label (line 12). However, the absence of evidence for failures does not mean correctness. This is indeed an important shortcoming for metamorphic-based random test generations. Our algorithm instead uses a statistical hypothesis testing to provide statistical confidence on the absence of failures, starting from the base test case.

The null and alternative hypotheses are

\[
\mathcal{H}_0 : \mathbb{P}(x_1) \geq \theta, \quad \mathcal{H}_1 : \mathbb{P}(x_1) < \theta
\]

where \( \mathbb{P}(x_1) \) is the probability that follow-up test cases, starting from \( x_1 \) as the source test, are passed, \( \theta \) is the lower-bound on the probability, \( \mathcal{H}_0 \) is null hypothesis, and \( \mathcal{H}_1 \) is the alternative. Our goal is to witness enough passed test cases to accept \( \mathcal{H}_0 \) as opposed to \( \mathcal{H}_1 \). There are multiple ways to conduct such statistical testing. The sequential probability ratio test and a Bayes factor are examples. We follow Jeffreys test [26], [27], a variant of Bayes factor, with a uniform prior to find a lower-bound on the number of successive samples \( K \) that sufficient for us to convince \( \mathcal{H}_0 \):

\[
K \geq \left(\frac{-\log B}{\log \theta}\right)
\]

where \( B \) in numerator is Bayes factor and can be set to 100 for a very strong evidence. For instance, to achieve a \( \theta = 0.95 \), we are required to set \( K \geq 90 \) to be highly confident on accepting \( \mathcal{H}_0 \). Lines 13-17 show this hypothesis testing.

After generating the test suite, our algorithm uses a data-driven approach to infer circumstances under which the software fails. Given the set of test cases with ‘passed’ and ‘failed’ labels, the problem appears to be a standard classification to discriminate between the two labels [28]. However, the generated samples are not independent of the follow-up samples are dependent on the base samples. To overcome this challenge and enable standard decision trees to provide intuitive explanations, we use a feature engineering technique to define two copies of features: base features and follow-up features (line 21). For example, for feature \( AGI \), we now have two features \( AGI_1 \) and \( AGI_2 \) for the evaluation of base and follow-up cases. Then, we combine the base and follow-up test cases to represent them with a single test instance. In the \( AGI \) example with \( AGI=10k \) for the base and \( AGI=12k \) for the follow-up test cases, we convert them into one test case with \( AGI_1=10k \) and \( AGI_2=12k \). This feature engineering enables us to directly infer decision tree models with an off-the-shelf algorithm (line 22).

VII. EXPERIMENTS

Implementations. We implement test-case generations in Python using the XML parser library to define the tax field variables and their domains. We instrument the tax preparation software using llvm-cov to collect code coverage information for each input trace (e.g., execution count of each line of code). We implement the decision trees in scikit-learn framework [29] using the CART tree library.

Environment and Setup. We run all the experiments on an Ubuntu 20.04.4 LTS OS sever with AMD Ryzen Threadripper PRO 3955WX 3.9GHz 16-cores X 32 CPU and two NVIDIA GeForce RTX 3090 GPUs. In Algorithm 1, we set \( B \) to 100, \( \theta \) to 0.95, \( \delta \) to 1.0, and \( T \) to 900.

Open-source Tax Preparation Software. We used four different versions of OpenTaxSolver [3] for the tax year 2018.
TABLE I: Metamorphic properties for five domains in the US tax policies. \(F\) is federal tax return where negative values mean the individual owns payment to the IRS, \(s\) is filing status, \(s_{lab}\) is spouse's field lab, \(MFJ\): married filing jointly, \(MFS\) is married filing separately, \(AGI\) is adjusted gross income, \(L2T\) is line 27 of IRS 1040 for Earned Income Tax Credit (EITC), \(QC\) is the number of qualified children, \(OD\) is the number of other dependents, \(CTC\) is child tax credits, \(L19\) is line 19 of IRS 1040 for Child Tax Credit (CTC), \(L29\) is line 29 of IRS 1040 for Education Tax Credit (ETC), \(MDE\) is medical/dental expenses reported in line 1 of schedule A, \(iz\) is to use itemized deductions \((ID)\) vs. standard deductions, and \(L12\) is total itemized deductions \((ID)\) from schedule A.

| Id | Domain | Metamorphic Property |
|----|--------|----------------------|
| 1  | Disability | \(\forall x,y((x,age \geq 65) \land (y,age \leq 65)) \lor ((x,blind \land y,blind) \lor (x,blind \land \neg y,blind)) \Rightarrow F(x) \geq F(y)\) |
| 2  | Disability | \(\forall x,y((x,age \geq 65) \land (y,age \leq 65)) \lor ((x,blind \land y,blind) \lor (x,blind \land \neg y,blind)) \Rightarrow F(x) \geq F(y)\) |
| 3  | EITC | \(\forall x,y(x,ets = MFJ \land x.L2T > y.L2T > 0) \Rightarrow F(x) = F(y)\) |
| 4  | EITC | \(\forall x,y(x,ets = MFJ \land x.AGI > 56,844) \Rightarrow F(x) = F(y)\) |
| 5  | EITC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 56,844 \land y.AGI > 56,844) \lor (x.L2T > 0) \land y.L2T = 0 \lor (x.L2T = 0) \land y.L2T > 0) \Rightarrow F(x) \neq F(y)\) |
| 6  | EITC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 56,844 \lor (x.L2T > 0) \land y.L2T = 0 \lor (x.L2T = 0) \land y.L2T > 0) \Rightarrow F(x) \neq F(y)\) |
| 7  | CTC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 200k \Rightarrow F(x) \leq F(y)\) |
| 8  | CTC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 200k \Rightarrow F(x) \leq F(y)\) |
| 9  | EITC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 200k \Rightarrow F(x) \leq F(y)\) |
| 10 | EITC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 200k \Rightarrow F(x) \leq F(y)\) |
| 11 | EITC | \(\forall x,y(x,ets = MFJ) \Rightarrow \forall y(x,ets = AGI) \land x.AGI \leq 200k \Rightarrow F(x) \leq F(y)\) |
| 12 | ID | \(\forall x,y((x,ets = MFJ) \land x.MDE = x.AGI \land y.MDE = y.AGI) \Rightarrow F(x) \leq F(y)\) |
| 13 | ID | \(\forall x,y((x,ets = MFJ) \land x.MDE = x.AGI \land y.MDE = y.AGI) \Rightarrow F(x) \leq F(y)\) |
| 14 | ID | \(\forall x,y((x,ets = MFJ) \land x.MDE = x.AGI \land y.MDE = y.AGI) \Rightarrow F(x) \leq F(y)\) |
| 15 | ID | \(\forall x,y((x,ets = MFJ) \land x.MDE = x.AGI \land y.MDE = y.AGI) \Rightarrow F(x) \leq F(y)\) |
| 16 | ID | \(\forall x,y((x,ets = MFJ) \land x.MDE = x.AGI \land y.MDE = y.AGI) \Rightarrow F(x) \leq F(y)\) |

The software includes the US individual federal tax return as well as the tax return computations for multiple US states (e.g., CA, MA, and NC). The functionalities used for computing the federal tax return include 6,017 lines of code for the tax year 2020. The number of input fields for the tax year of 2018, 2019, 2020, and 2021 are 92, 100, 110, and 187, respectively. Many of these fields are real numbers, but a few fields are binary and categorical.

**Research Questions.** We seek to answer the following three questions using our tool TENFORTY in the defined setup.

- **RQ1.** Are metamorphic relations useful to capture the legal requirements of tax preparation software?
- **RQ2.** Can randomized algorithm with Bayesian guarantees be effective in testing tax preparation software against the metamorphic specifications?
- **RQ3.** Could fault localization techniques help pinpoint the root of failures in the internal and input spaces?

The source code and implementation of TENFORTY is available at: https://github.com/Tizpaz/TenForty

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A. Metamorphic Relations (RQ1)

**Tax Policies.** We consider aspects of the U.S. Individual Income Tax Return that relate to disability, credits, and deductions. These domains are known to be notoriously challenging [15]. We focus on fields related to the standard deductions for senior and disable individuals; Earned Income Tax Credit (EITC) [25], a refundable tax credits for lower-income households; Child Tax Credit (CTC), a nonrefundable credits to reduce the taxes owed based on the number of qualifying children under the age of 17 [30]; Educational Tax Credit (ETC) that help students with the cost of higher education by lowering their owned taxes or increasing their refund [31]; and Itemized Deduction (ID) that is an option for taxpayers with significant tax deductible expenses [32].

**Metamorphic Relations.** We use scenarios and examples described in these policies to synthesize metamorphic relations. Table I shows 16 metamorphic relations in 5 domains for the tax year 2020. For properties #9 to #12, we assume \(MAGI\) (modified adjusted gross income) is equivalent to \(AGI\) [33]. Next, we provide a brief explanation of some of these properties.

- **Property #1.** A senior (over age of 65) or bind individual must receive similar or better tax benefits when compared to a person without the disability or seniority who is similar in every other aspect (due to higher standard deductions for seniors and blind).
- **Property #2.** An individual with the married filing jointly \((MFJ)\) status with a disabled/senior spouse must receive similar or higher tax benefits compared to a similar individual but without the disabled or senior spouse.
- **Property #3.** An individual with the married filing separately \((MFS)\) status is ineligible for EITC in 2020.
- **Property #4.** An individual with the married filing jointly \((MFJ)\) status with \(AGI\) over 56,844 is ineligible for EITC in 2020.
- **Property #5.** An individual who qualifies for EITC must receive a higher return than a similar unqualified one.
– Property #6. Among two qualified individuals with EITC, one with higher EITC claims receives higher or equal benefits.

– Property #7. Among two qualified married filing jointly (MFS) individuals, one with higher child tax credits receives higher or equal tax return benefits.

– Property #8. This 4-property requires a comparison between four “similar” individuals since there is a relation between two variables of interests: AGI and the number of qualified children/others to claim a CTC. An individual with more qualified dependents must receive higher or similar tax return benefits than an individual with fewer dependents after adjusting for the effects of income levels on the calculations of both the final return and the amounts of CTC claims. Expressing this property requires holding the income of two individuals the same per each qualified number of children/others.

– Property #9. An individual with the married filing separately (MFS) status is ineligible for ETC in 2020.

– Property #10. An individual with the married filing jointly (MFS) status with AGI over 180k is ineligible for ETC.

– Property #11. A qualified individual with AGI below 160k who claims ETC received higher or similar tax return benefits compared to a similar individual who is ineligibility or does not claim ETC for the tax year 2020.

– Property #12. This 4-property requires a comparison between four “similar” individuals as the rule changes for individuals with AGI below 160k and between 160k and 180k. By holding AGI constant between two individuals with AGI below 160k (varying the ETC claims) and two individuals with AGI between 160k and 180k (varying the ETC claims with the same rate), the property requires that individuals with lower income (below 160k) receive higher or similar tax returns.

– Property #13. An individual who files with medical/dental expenses (MDE) below 7.5% of their AGI and itemizes their deductions receives the same return as a similar individual with no MDE claims.

– Property #14. When filing with a standard deduction, total itemized deduction (Line 12) must have no effect on the tax returns.

– Property #15. An individual who files with itemized deductions below the standard deductions receive a lower or similar tax return benefits compared to a similar individual who used the standard deductions.

– Property #16. An individual who files with itemized deductions above the standard deductions receive a higher or similar tax return benefits compared to a similar individual who claims standard deductions.

Metamorphic Relations in Different Years. As the tax law has evolved over different years, the metamorphic relations need to be updated to reflect those changes. Table II shows the modified metamorphic relations with respect to the tax year 2020. These are some important changes:

1) Unlike previous years, married filing separately is qualified for EITC as reflected in property #3 for the tax year 2021.

2) The AGI eligibility were different for different years as reflected in properties #4, #5, and #6.

3) In the version 2018 and 2019, the software does not allow users to check whether they itemize deductions. Therefore, we cannot specify the property #14 for these two years.

4) In the version 2018 and 2019, by not allowing for choosing itemized deductions, the software should automatically pick the option (standard vs. itemized) that maximizes the taxpayer benefits. Therefore, the modified property #15 makes sure that software chooses standard deductions when the itemized deductions are lower. Similarly, property #16 validates that the software uses itemized deductions when those deductions are higher.

We also observe that the U.S. Individual Income Tax Return is getting more complicated each new year. For example, the software version 2018 takes 92 input fields, whereas the version 2021 takes 187 input fields.

Answer RQ1: We found that metamorphic relations are suitable to specify the correctness requirements in tax preparation software. Furthermore, these relations allow us to update the requirements as the tax policies are evolving with minimal effort.

B. Test-Case Generations (RQ2)

We implement the Algorithm 1 in TENFORTY to generate base and follow-up test cases and find the evidence that the software fails to satisfy the metamorphic requirements. In doing so, we find inputs that satisfy the premises, but it negates the conclusion of metamorphic relation. We run each experiment 10 times, each for 15 minutes (the results are averaged over these repeated runs).

Table III shows the results of random test-case generations. We organize the table into four parts for the tax year 2018, 2019, 2020, and 2021, respectively. As we discussed previously, we cannot specify the metamorphic relation for ID (14), hence we skip this property for testing of software versions 2018 and 2019. We report the number of generated test cases, the number of passed ones, the number of failed cases, and the

| Id | Year 2018 | Year 2019 | Year 2021 |
|----|-----------|-----------|-----------|
| 1,2| No Change | No Change | No Change |
| 3  | No Change | No Change | 4 \( x \cdot AGI > 54, 884 \) \( y \cdot AGI > 55, 952 \) \( z \cdot AGI > 57, 141 \) |
| 4  | x \cdot AGI > 54, 884 \( y \cdot AGI > 55, 952 \) \( z \cdot AGI > 57, 141 \) |
| 7-13| No Change | No Change | No Change |
| 14 | Not Possible | Not Possible | No Change |
| 15 | x \cdot L \( x \cdot L \cdot AGI > 24, 06 \) ≤ \( F(x) \cdot F(y) \) ≤ \( F(x) \cdot F(y) \) ≤ \( F(x) \cdot F(y) \) |
| 16 | x \cdot L \( x \cdot L \cdot AGI > 24, 06 \) ≤ \( F(x) \cdot F(y) \) ≤ \( F(x) \cdot F(y) \) ≤ \( F(x) \cdot F(y) \) |

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time to observing the first failed case (in seconds). Overall, we found that our search strategy is efficient that generates over 36,000 test cases for 2-property relations and 17,000 for 4-property relations in average. We also found that the testing technique can often find the first evident of failures within a few seconds and up to 70 seconds in the worst-case.

**Different Variant of Software.** As the tax law evolves in the response to ever-changing politico-economic realities, the tax preparation software has to be adapted to reflect those changes. Our experiences with metamorphic testing show that the tax preparation software might not be properly updated to account for those changes. In particular, we did not find any evidence of failures for all 16 properties for 2018 and 2019 versions, whereas there is evidence of failures for 2020 and 2021 versions. One specific example is property #4 where the software satisfies the property for 2018 and 2019, but it fails for 2020. Upon further investigation, it seems that the software has not been updated to reflect the new eligibility based on the annual growth income (see Id=4 in Table II). Another interesting finding is for property #3, comparing the tax years 2020 and 2021. For the tax year 2020, the status of married filing separately (MFS) was not eligible for earned income tax credits (EITC); however, this status has become eligible for EITC in tax year of 2021. While, the 2020 version failed to satisfy property #3, the 2021 version (without any updates) satisfies this property, solely due to the updated policy.

**Failed Metamorphic Relations.** We found test cases that violate the correctness requirements for the 2020 and 2021 versions of software. One area that software shows weakness is the filing status of married filing separately (MFS) where two properties (properties #3 and #9) out of three correctness specifications for this status (properties #3, #7, and #9) are failed. While, the majority of filing are single or married filing jointly, the MFS status is still an important class of filing for taxpayers in the US when 3.07 million people used this status to file their taxes in 2016 (out of 150.3 million federal returns filed). Another area of vulnerability is the annual growth income (AGI) that influences the correctness of software in many specifications (9 properties out of 16 have some conditions on the AGI). Since the eligibility based on AGI has consistently been modified by IRS in different years (see Table II), it is critical to take into account a design that requires minimal efforts to update conditions for different computations (e.g., EITC, CTC, and ETC).

**Answer RQ2:** We found that our proposed random search algorithm is effective and efficient in exploring the space of tax preparation software to uncover failures. Our experiences revealed multiple areas where updated software is no longer satisfying the correctness requirements. In addition, our experiments showed multiple weakness areas relate to married filing separately status and the maximum annual growth income.

### C. Fault Localization (RQ3)

In this section, we investigate whether decision tree artifacts are expressive and useful to aid tax preparation software developers and users in explaining and debugging different correctness properties. We first use a simple example of disability (properties #1 and #2) to showcase the usefulness of decision tree artifacts. Then, we focus on the properties that have failed to satisfy the metamorphic correctness requirements to explain and localize root causes.

Figure 2 (left) shows five clusters of federal tax returns (FTR) obtained by varying four disability/senior conditions (age above 65, blindness, spouse age over 65, and spouse blindness). Since there are 16 possibilities for these four Boolean conditions, our goal is to infer a decision tree model that explains what conditions are similar within each cluster and what conditions distinguish different clusters from each other. Figure 2 (right) shows the corresponding DT model for explanations. Each path from root nodes to the leaf defines a condition on inputs such that if any input satisfies the condition, it assigns to the corresponding cluster label of leaf node. For example, the lowest orange cluster (FTR below $1,600) is explained by a condition where their age and their spouse’s age are less than 65, and none of them are blind. The second cluster from below (Brown color with the FTR a bit above $1,700) is explained by four paths where the taxpayer has one disability/senior condition out of four possibilities. The third cluster from below (blue) is described by six paths
where the taxpayer has two disability/senior conditions. In a similar fashion, the next two clusters have three and four disability/senior conditions out of four possibilities. Therefore, the decision tree shows that the number of “yes” answers to four senior/disability (age above 65, blindness, spouse age over 65, and spouse blindness) explains the five clusters found in the Federal Tax Return.

**Explanations in the input space.** TENFORTY uses a similar technique to explain circumstances on the input variables (different items in the tax return) under which the software fails to satisfy the metamorphic properties. We label failed test cases with orange colors and passed ones with green colors. Note that if all test cases are failed, we just report the premises of the corresponding metamorphic property, and it means the software completely miss those conditions. Otherwise, we provide debugging supports via decision tree artifacts.

Table IV (second column) shows explanations in the input space of software. We note that features ending with _1 are bases and _2 are follow-ups (for 4-properties, features ending with _1 and _2 are bases and _3 and _4 are follow-ups).

For EITC (3), the decision tree shows that the software fails in all cases excepts when the annual growth income (AGI) is less than $16,720 and the federal tax return (FTR), shown with return, is less than $79. In other words, the software fails to enforce property #3 in Table I in all cases, except for cases with a federal tax return of less than $80. For ETC (9), the decision tree shows that the software also fails to satisfy the metamorphic requirements in all cases, except when the tax return becomes zero. We conjecture that the correct cases are due to numeric approximations as the computations are expected to use a small non-zero value, but are approximated due to the finite precision. Therefore, the software is correct for those cases solely because of numerical errors. Similarly, for ETC (11) and ID (16), the software satisfies the properties in the majority of cases but fails in a few corner cases. Inspecting these failures, we found that they also include an interval of FTR with zero return. So, the software behaves erroneously due to numerical approximations, but is correct otherwise. For ID (13), the decision tree model shows circumstances over the medical expenses (the first line of schedule A shown with A1 and the MDE variable) and the return. The software fails when the medical expenses are over $13,487 and the tax payer opts to itemize deductions (A18 is set to true). In other words, the software behaves correctly if the user does not itemize, but becomes faulty when the user opts for itemized deduction. We conjecture that this is due to the fact that the 2020 version was updated to allow users to opt for standard versus itemized deductions, which were not possible in past versions. But, the updates might not be properly implemented for all corner cases and let users take deductions when they opt for itemized deduction, but do not meet the eligibility conditions.

**Explanations in the internal space.** We further extend TENFORTY to aid tax preparation software developers to debug their code. In particular, we collect internal traces of each execution such as how many times a loop is executed, what branch in an if condition is taken, and what case in a switch statement is executed. We use the same label as the debugging in the input space where each traces is labeled as passed (green) and failed (orange), and we want to localize program internal properties that distinguish failed traces from passed ones. The decision trees learned over program internal features are shown in the third column of Table IV.

As an example, let us consider EITC (3). The failed and passed test cases are distinguished based on the number of iterations of while loop in line 93 and whether the tax computation ends up refunding a return to the user in line 2156 with the variable L[34]. For another example, the decision tree model for ETC (11) pinpoints to an if condition and a switch statement in line 423 and 340, respectively.

**Answer RQ3:** We found that decision trees are useful artifacts to explain circumstances under which the tax preparation software fails to satisfy the metamorphic requirements. Our experiences reveal that (i) the software might completely miss an eligibility condition, (ii) finite precision in the computation might lead to unexpected errors, and (iii) the updated version allows users to opt for an option might not consider all cases, especially the corner ones.

**VIII. RELATED WORK**

**Tax Preparation Software.** Merigoux et al. [34] developed a compiler for the French tax code. They pointed out multiple limitations of M programming language, developed by
French Public Finances Directorate to write tax rules (available at [35]). Then, they developed a domain-specific language that allows for specifying complicated rules and lifting them to modern languages like Python. They also used a dynamic random search to validate the software, as opposed to formal verification, due to the large space of inputs, floating-point computations, and various optimizations. In comparison, the US has much less automation in tax preparation with no available specifications and regulated test cases. Yu, McCluskey, and Mukherjee [36] proposed knowledge-based graphs to personalize the tax preparation within the TurboTax software. In addition, SARA [37] translated the statutes into Prolog programs and the cases into Prolog facts, such that each case can be answered by a single query. Alternatively, they proposed to adapt high-dimensional natural language processing techniques such as Legal BERT to overcome some of intrinsic limitations of logic-based programming.

**Fairness.** Algorithmic fairness is an important area to promote inclusion, diversity, and accessibility of software solutions [38], [39], [40]. Within the tax domain, Black et al. [10] studied fairness of algorithmic tax audit selections by the United States Internal Revenue Service (IRS) from 2010-14 using the concept of vertical equity. They found that flexible machine learning with higher accuracy, as opposed to simpler ones, may undermine vertical equity by shifting tax audit burdens from high-income to middle-income taxpayers. They also pointed out multiple weaknesses in applying existing fairness solutions to the tax audit problems. Finally, they made multiple suggestions to improve the vertical equity through fair audit selection. Other articles also made similar observations that the IRS might audit low-income taxpayers at the same rate as the richest taxpayers [41], [42], [43]. For example, a ProPublica article reported that the top 1% of taxpayers by income were audited at a rate of 1.56% whereas earned income tax credit (EITC) recipients, who typically have an annual income under $20,000, were audited at 1.41% in 2018. Multiple works also pointed out the issue of “color-blind” tax code in the US [44], [45], [46]. Moran [44] used the horizontal equity as fairness notion that requires similarly situated taxpayers should have taxed similarly. The study found that blacks and whites who are similar by income are not taxed similarly because they fundamentally have different lifestyles. Studying fairness and ethical aspects of tax law as implemented in a tax preparation software system is an interesting future direction.

Beyond the US tax system, a Dutch digital welfare fraud detection system, known as SyRI, is ruled to be unlawful since it does not comply with the right to privacy under the European Convention of Human Rights and the European Union General Data Protection Regulation (GDPR). Furthermore, the court found that the SyRI legislation is insufficiently transparent and verifiable and brings risks of discrimination [47].

**IX. Broader Impacts**

Although most of our technical discussion focused on the US-based tax preparation software, the key takeaway is on the importance of metamorphic relations for the sociolegal software. We discuss two examples highlighting this connection.

**Legal-Critical Software.** Let us first consider the work by Matthews et al. [48], [49] on forensic DNA software that aims to understand the role of black-box forensic software in moral decision-making in criminal justice. They conduct independent testing of Forensic Statistical Tool (FST), a forensic DNA system developed in 2010 by New York City’s Office of
Chief Medical Examiner (OCME). Using a collection of over 400 mixed DNA samples, they found that an undisclosed data-dropping method in software impacts about 25% of the samples and leads to shifted results toward false inclusion of individuals who were not present in an evidence sample. The techniques developed in our paper may allow one to uncover such vulnerabilities without having an access to DNA samples purely on the basis of an appropriate metamorphic query uncovering differential data-dropping.

Socio-Critical Software. Escher and Banovic [50] studied errors in poverty management systems that are critical tools to support vulnerable populations. Online benefits screening tools advise households about their eligibility before proceeding with full applications. Hence, an error in such a system can deprive qualified families from receiving the benefits they are entitled to. Escher and Banovic developed a framework to test an instance of such screening tools as implemented in the Pennsylvania “Do I Qualify?” website [51]. They took the benefit eligibility handbook [52] and implement their own screening software. Then, they use census data to generate test households and compare the results of the online tool against their own implementations. Taking their own implementations as the ground truth, they mark any discrepancies as errors. Overall, they found major errors in the implementation of the tool that can be used as necessary correctives to fix them to improve accessibility for the most vulnerable populations.

Metamorphic testing again can complement this approach by eliminating the need for a comparative implementation.

X. CONCLUSION

Tax preparation software are increasingly indispensable in navigating the complex tax structure. Since the legal responsibilities of bugs in such software rest on the end-users, most of whom cannot afford expensive accountants or commercial software, developing debugging aids for such systems is our social responsibility. We presented a data-driven debugging framework for metamorphic specifications expressed in a first-order logic. We hope that our experience in capturing the tax-preparation software requirements can convince the reader that the metamorphic specifications are both intuitive and unambiguous in expressing the comparative nature of legal requirements. The experimental results demonstrated that search-based software engineering approaches are useful in uncovering and explaining bugs in a popular open-source tax preparation software.

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