Latent Fingerprint Registration via Matching Densely Sampled Points
Shan Gu, Student Member, IEEE, Jianjiang Feng, Member, IEEE, Jiwen Lu, Senior Member, IEEE, and Jie Zhou, Senior Member, IEEE

Abstract—Latent fingerprint matching is a very important but unsolved problem. As a key step of fingerprint matching, fingerprint registration has a great impact on the recognition performance. Existing latent fingerprint registration approaches are mainly based on establishing correspondences between minutiae, and hence will certainly fail when there are no sufficient number of extracted minutiae due to small fingerprint area or poor image quality. Minutiae extraction has become the bottleneck of latent fingerprint registration. In this paper, we propose a non-minutiae latent fingerprint registration method which estimates the spatial transformation between a pair of fingerprints through a dense fingerprint patch alignment and matching procedure. Given a pair of fingerprints to match, we bypass the minutiae extraction step and take uniformly sampled points as key points. Then the proposed patch alignment and matching algorithm compares all pairs of sampling points and produces their similarities along with alignment parameters. Finally, a set of consistent correspondences are found by spectral clustering. Extensive experiments on NIST27 database and MOLF database show that the proposed method achieves the state-of-the-art registration performance, especially under challenging conditions.

I. INTRODUCTION

Latent fingerprints have been playing a vital role in identifying suspects [1]. Up to now, manual feature extraction and matching is still indispensable in latent fingerprint matching. Recently, automatic latent fingerprint feature extraction and matching has become a research focus in the field of fingerprint recognition, aiming to reduce the workload of fingerprint experts. Despite of many published work on this topic, the recognition performance degrades greatly when the latent fingerprint has small effective area, low image quality or large distortion [2]. Therefore, there is still large room for improvement in latent fingerprint matching.

In latent fingerprint matching algorithms, accurate fingerprint registration is of vital importance for the recognition performance. Minutiae based methods [4, 5] are most commonly used to establish correspondences across images, which first extract minutiae from each fingerprint, then extract minutiae descriptors, and finally use them to find reliable matches. Among the three steps, accurate extraction of minutiae is the basis, which will greatly affect the accuracy of the subsequent steps. However, the requirement that sufficient and accurate minutiae is usually difficult to meet for latent fingerprints with low quality. The estimated minutiae may be very few when the latent fingerprints have small effective area or inaccurate in location or direction when fingerprint images are greatly occluded by background noise. Fig. 1 shows an example in NIST27 database [6], where none of minutiae extracted by FingerNet [3] is correct. The proposed method can find sampling point correspondences under such challenging situation.

The authors are with the State Key Laboratory of Intelligent Technologies and Systems, Beijing National Research Center for Information Science and Technology (BNRist), Beijing 100084, China, and also with the Department of Automation, Tsinghua University, Beijing 100084, China. (Email: gus16@mails.tsinghua.edu.cn; jfeng@tsinghua.edu.cn; lujiwen@tsinghua.edu.cn; jzhou@tsinghua.edu.cn)
Fig. 2. The flowchart of the proposed fingerprint registration system. Here shows only one stage in the coarse-to-fine registration scheme, and the whole registration system contains two registration with different resolutions. Sampling points are first sampled uniformly in the ROI on each fingerprint, where the ROI of latent fingerprint is manually marked, and that of rolled fingerprint is estimated by FingerNet [3]. The sampling intervals on the latent and rolled fingerprint are $32 \times 32$ and $64 \times 64$, respectively. Then the proposed patch alignment and matching method compares all pairs of sampling points, adjusts the relative location and direction of sampling points on the latent fingerprint, and computes their similarities. Sampling point pairs whose similarity are higher than a given threshold are considered potential correspondences. The spectral clustering based global patch matching method is finally applied to find a set of compatible corresponding sampling points among all potential correspondences.

ridge orientation as the direction. With virtual minutiae, the following matching procedure is similar with minutiae based approaches. The virtual minutiae based method can alleviate the problems of insufficient minutiae caused by small area or poor quality, but it still suffers from unstable estimation of local ridge orientation, which is common in latent fingerprints. The wrong estimation of direction of virtual minutiae will greatly affect the performance of virtual minutiae descriptors since the descriptor is extracted from local image patch aligned with the direction. Another limitation is that virtual minutiae are not salient features and cannot be located accurately, so the accuracy of fingerprint registration is limited by sampling intervals. To achieve registration accuracy at the pixel level, this method needs to take each pixel as a sampling point, which has very high computational complexity and is impractical.

In this paper, a new latent fingerprint registration algorithm based on dense sampling points is proposed. Fig. 2 shows its flowchart. The proposed method can further enhance the anti-noise ability of registration algorithms and has high efficiency, which is attributed to the following designs.

The core of the proposed registration algorithm is local patch alignment and matching. Fingerprint is represented as dense sampling points in replace of minutiae to avoid minutiae extraction step and ensure the adequacy of key points even if fingerprints area is very small. It should be noted that we do not refer to them as virtual minutiae because we do not estimate their directions. Then the local patch alignment and matching algorithm estimates the alignment parameters between image patches and computes their similarities. Its flowchart is illustrated in Fig. 3. Compared with previous minutiae or virtual minutiae based registration, we add the local patch alignment module before extracting sampling point descriptors, which is key to handle their limitations. Concretely, (1) the estimation of relative rotation between two sampling points rather than separate estimation of their own local direction helps two patches aligned more accurately in rotation. (2) The estimation of relative offset between two sampling points helps the algorithm achieve pixel-level accuracy without the need of sampling every pixel. In addition, the proposed local patch matching module computes the similarity of two original image patches rather than enhanced ones to ensure that the image will not be damaged by the fingerprint enhancement algorithm. In conclusion, we skip the traditional fingerprint feature extraction framework of extracting level-1 (ridge orientation and frequency) and level-2 (minutiae) features and thus avoid being affected by errors in feature extraction.

After that, potential correspondences between sampling points are obtained by comparing their similarities to a predefined threshold. Since there are still a large number of false correspondences, spectral clustering based global patch matching is proposed to find a set of consistent corresponding sampling points.

Considering registration accuracy and time complexity, an coarse-to-fine registration scheme is proposed. The registration algorithm in both stages is the same, and the precise registration takes the result of coarse registration as input. In coarse registration stage, the sampling interval is large, and all pairs of sampling points on two fingerprints are considered for comparison. In precise registration, the sampling points are denser, but each sampling point is compared only with its neighbors. With such a scheme, large amount of comparison in coarse registration is required but the number of sampling points is small while in precise registration the sampling points are denser but the number of matches required for each point decreases.

Extensive experiments on latent fingerprint registration are conducted on NIST27 database [6] and MOLF database [9]. On NIST27 database, the distances between manually marked matching minutiae after registration are used as the evaluation
Fig. 3. The flowchart of the proposed local patch alignment and matching algorithm. Given two image patches (from latent and rolled fingerprints) centered on the sampling points, the patch alignment module predicts the spatial transformation $\theta_{\text{predict}}$ between them. With the predicted transformation, the latent fingerprint patch are well aligned to the rolled fingerprint patch. After alignment, each image patch is represented as a deep descriptor, and the similarity between descriptors is outputted to reflect how similar the two patches are, and meanwhile whether the two sampling points are corresponding points.

metric. The experimental results show that our approach performs better than existing methods and especially under challenging conditions such as heavy background noise and small fingerprint area.

The rest of the paper is organized as follows. In Section 2, we review the related work. In section 3, we illustrate the proposed latent fingerprint registration method including the details of local patch alignment and matching, and global patch matching. In Section 4, we evaluate the performance of the proposed registration method. In Section 5, we conclude the paper.

All kinds of fingerprint registration algorithms can be regarded as key point-based registration algorithms when we view minutiae, ridge sampling points, image sampling points, sweat pores, and even pixels as key points. In the following, we review several representative work pertaining to different modules including the selection of key points, descriptors, and global registration.

A. Key Points

The key points in registration algorithms contain minutiae, sampling points on ridges, sampling points on image, sweat pores, and pixels. Minutiae [4, 5] are the most commonly used since it is greatly distinctive and can be extracted robustly on high quality fingerprints. However, minutiae are still sparse and can not generate very precise registration results when fingerprints are distorted.

To improve the registration performance, a lot of work combines minutiae with other key points. In order to better deal with distortion, sampling points on ridges [10, 11], undirected sampling points on images [12], and pixels [13] are aligned after initial minutiae registration. For high resolution fingerprints, level 3 features [14] including pore and ridge contours are extracted as key points, which can boost the performance when combining with minutiae registration. In latent fingerprints which are usually with low quality, minutiae and ridges may not be accurately extracted. To solve this problem, Cao et al. [7, 8] proposed virtual minutiae (directed sampling points on images) to ensure enough key points on fingerprint area. But their direction may be mis-estimated, which would affect the matching performance.

In this paper, we adopt dense undirected sampling points on images to ensure adequate key points and do not define their absolute direction to avoid possible error of direction estimation. Besides, different from the method in [12], our method does not require minutiae registration as initialization.

B. Descriptors

Descriptors are very important for identifying whether two key points match or not. Minutiae descriptors have been widely researched, and the descriptors for other key points are similar with them. Therefore, we discuss minutiae descriptors in the following.

Traditional minutiae descriptors can be divided into three categories: image based, texture based, and minutiae based descriptors. Image based [15, 16] and texture based [17, 18] descriptors use image intensity or ridge orientation information, while minutiae based descriptors [19–24] make use of the relationships between neighboring minutiae. These methods use manually designed features and thus are difficult to optimize to separate mated minutiae pairs from non-mated pairs, especially under challenging situations.

Recently, descriptors constructed by deep learning [7, 8, 25, 26] are proposed to capture the essential characteristics of fingerprint patches. To ensure the robustness of descriptors, local image patches are aligned in advance based on their estimated key point direction. Experiments show their superior performance compared to traditional descriptors. However, their performance may be degraded when image patches are aligned with wrong direction. Besides, since these methods use enhanced fingerprints as input, it may also cause performance degradation when images are enhanced with wrong ridge orientation, which is common in latent fingerprints.

In our method, we align the latent image patches with estimated spatial transformation relative to rolled image patches before extracting their deep descriptors. The deep descriptors are learned from original image patches rather than enhanced ones, which avoid being affected by errors in ridge orientation estimation.
Fig. 4. Sampling points on a pair of fingerprints (has undergone coarse registration) in the precise registration stage. The sampling intervals on both fingerprints are $16 \times 16$. A sampling point on the latent fingerprint (marked in yellow in (a)) is only compared with neighboring sampling points (marked in yellow in (b)) on the rolled fingerprint.

Fig. 5. The model architecture of the proposed patch alignment algorithm.

Fig. 6. The model architecture of the proposed deep descriptor.

**II. RELATED WORK**

**A. Global Registration**

Minutiae based approaches usually fit a thin-plate spline model with paired minutiae as landmark points. The correspondences between minutiae are established by considering both similarity of minutiae descriptors and compatibility between minutiae pairs [27, 28]. Cao et al. [7] introduced the compatibility between minutiae triplets to further eliminate false correspondences.

Many non-minutiae based methods [10, 12, 13] use minutiae registration as an initial step because minutiae are significant key points, and their small number leads to high matching efficiency. However, incorrect minutiae registration will result in incorrect initial registration of these methods.

Our method takes sampling points as key points and does not use minutiae registration as initialization in order to improve the performance of low quality images and small area fingerprints. We establish the initial correspondences according to the similarities between sampling point pairs and use the pairwise geometric constraints to select a subset of consistent correspondences by spectral clustering.

**III. PROPOSED REGISTRATION ALGORITHM**

In this section, we introduce in detail the proposed registration algorithm, including the proposed local fingerprint patch alignment, the local patch matching, the global patch matching, and implementation details of all methods.

**A. Coarse-to-fine framework**

In order to balance registration accuracy and time complexity, the proposed approach applies a coarse-to-fine latent fingerprint registration framework. It contains two stages: coarse registration and precise registration. The registration process in both stages is the same, but the acquisition and matching of sampling points are different.

In coarse registration stage, original pairs of fingerprints are taken as input. The sampling intervals on rolled fingerprints are $64 \times 64$, while that on latent fingerprints are $32 \times 32$ due to small fingerprint area. We compare all the sampling points on latent fingerprints with those on rolled fingerprints to find the coarse correspondences.

In precise registration stage, we take registered fingerprints after coarse registration as input. The sampling intervals on both fingerprints are $16 \times 16$ considering both the preciseness and efficiency. Since the distance between corresponding points may not be too far after coarse registration, the sampling points on latent fingerprints are only compared with those on their neighbor on rolled fingerprints. An example of comparison is shown in Fig. 4.

**B. Local Patch Alignment**

Since sampling points are sampled separately on each fingerprint, it is difficult to correspond two sampling points directly on two fingerprints. One sampling point on the rolled fingerprint may correspond to one point on the latent fingerprint between two sampling points. Therefore, it is necessary to adjust the location and direction of sampling points on latent fingerprints to obtain the accurate correspondences. The patch alignment approach is proposed to estimate the relative spatial transformation between two image patches. Based on the estimation, the location and direction of sampling points are adjusted for better alignment.

We train a Siamese network to estimate the geometric transformation following [29]. The network architecture contains
three parts. The feature extraction network extract feature maps from image patches centered on two sampling points. Taking these two feature maps as input, a matching layer matches them and outputs a correlation map. With the correlation map, the translation and rotation parameters are estimated with a regression network.

1) Model Architecture: The flowchart of patch alignment algorithm is illustrated in Fig. 5. For the feature extraction network, we use the standard VGG-13 network and crop it before the pool4 layer. It has four double-conv blocks, and the first three are followed by a max pooling layer. Each double-conv block contains two conv layers where each conv layer followed by a BatchNorm layer and a ReLU layer. To overcome different appearances of input images, we add a ridge orientation supervision to help the network pay more attention to fingerprint ridges rather than the image background. We add the supervision layers at pool3, and let the network learns to estimate the orientation field. The supervision layers are made of a deconv layer, a double-conv block, a conv layer, and a Tanh layer.

After each image patch produce its feature map, the matching network is developed to combine two feature maps to a single one for the subsequent parameter estimation. We use a matching procedure similar to [29]. The correlation layer computes all pairs of similarities between feature maps and is followed by similarity normalization.

Given the correlation map, a regression map is applied to estimate the translation and rotation parameters between two image patches. The regression network is composed of two double-conv blocks and one fully connected layer. The output is 3-D vector, which indicates the relative translation in horizontal and vertical directions, and the relative rotation angle, respectively.

2) Loss Function: We train the patch alignment network in a fully supervised manner. For a pair of input image patches, the ground truth transformation parameter is given by \( \theta_{gt} = [dx, dy, da] \), indicates the relative translation and rotation angle. With the estimated parameter \( \theta_{pred} \), we use MSE loss to evaluate the parameter regression error:

\[
L_{para}(\theta_{gt}, \theta_{pred}) = \frac{1}{N} \sum_{i=1}^{N} ||\theta_{gt}^i - \theta_{pred}^i||^2
\]  

For the ridge orientation estimation, we also use the MSE loss for convenience. For an image patch of size \( H \times W \), the corresponding ground truth orientation map \( M_{gt} \) is a two-channel image map concatenating the cosine map \( \cos(2O) \) and sine map \( \sin(2O) \) of origin orientation field \( O \) whose size is \( \frac{H}{2} \times \frac{W}{2} \). The MSE loss for one input image patch is

\[
L_{ori}(M_{gt}, M_{pred}) = \frac{1}{N} \sum_{i=1}^{N} ||M_{gt}^i - M_{pred}^i||^2
\]

The final loss is a weighted sum of the loss of transformation estimation and the total loss of ridge orientation estimation for two input image patches, which is

\[
L_{match} = L_{para} + \lambda_{match}(L_{ori}^1 + L_{ori}^2)
\]

where \( \lambda_{match} \) is the weighted coefficient.

3) Simulation of Training Data: Training models in the fully supervised manner requires pairs of image patches and their corresponding transformation parameters. We prepare the training data by applying synthetic transformations to real pairs of latent and rolled fingerprints, which makes it easier to get large amount of data for the CNN training. See Section D for information on the used fingerprint database.

To synthesize the training data, the latent fingerprints are required to register to their paired rolled ones. We register two fingerprints based on the MCC descriptor [21] and spectral clustering [30]. The MCC is used to measure the similarity between all possible minutiae pairs, and spectral clustering is used to obtain the mated minutiae pairs. Based on the paired minutiae, Thin Plate Spline (TPS) [31] model is applied to approximate the distortion field. In order to ensure the correctness of training samples, we apply quality control manually to choose only examples whose registration is correct. Then we cut pairs of image patches whose size is \( 160 \times 160 \) randomly on the registered image pairs. Only pairs of image patches with common foreground area greater than a predefined threshold are preserved. In this way, we can obtain multiple pairs of aligned image patches from each pair of latent and rolled fingerprints. For a pair of image patch \( I_A \) and \( I_B \), random translation and rotation are applied to them, and the transformed patches are named as \( \hat{I}_A \) and \( \hat{I}_B \). We take the patch pair \( (I_A, \hat{I}_B) \) and \( (\hat{I}_A, I_B) \) as training pairs. The image patches in the latter pair are both from rolled fingerprints, which can make the network easier to train.

Specifically, we generate two training datasets for the coarse and precise registration, respectively. The parameter dimensions of the transformations are different in two datasets. In
Fig. 8. The proposed fingerprint simulation consists of two steps.

coarse registration, the range of random translation is \([-40, 40]\) pixels, and that of rotation is \([-40, 40]\) degrees, while in precise registration all the range is set as \([-20, 20]\). When training models, the parameters of translation are transformed to \([-1, 1]\), and rotation angles are converted to radian.

C. Local Patch Matching

The proposed local patch matching procedure aims to compute the similarity between a pair of aligned image patches. To compute the similarity, we extract deep descriptor from image patches centered on each sampling point, and take the distance between two descriptors as the patch similarity. We train a Siamese network to extract deep descriptors. Although minutiae descriptors based on depth learning have been proposed, our main contribution is to propose a dedicated process to address the problem of lacking of ground truth data. Simulating multiple fingerprints from rolled fingerprints can simultaneously solve the problem about the lack of samples and correspondence information.

1) Model Architecture: The VGGNet-13 architecture is adopted for the feature embedding. Similar with the feature extraction network in the proposed patch alignment algorithm, the supervision is added after pool3 to let the ridge orientation as supervisory information. After all the conv layers, the FC-BN structure is applied to obtain a 512-dimensional feature, which is used as the descriptor. The concrete architecture is illustrated in Fig. 6.

2) Loss Function: Similar with the loss in local patch alignment algorithm, the loss function here contains two parts, the contrastive loss \(L_{\text{contrastive}}\), which minimizes the distance between positive pairs while maximizes that of negative pairs, and the MSE loss \(L_{\text{ori}}\) which evaluates the estimation accuracy of ridge orientation. The total loss is

\[
L_{\text{simi}} = L_{\text{contrastive}} + \lambda_{\text{simi}}(L_{\text{ori}}^1 + L_{\text{ori}}^2)
\]  

where \(\lambda_{\text{simi}}\) is the weight coefficient.

3) Simulation of Training Data: To train the descriptor learning network, multiple samples are required for the same key point to enhance the generalization of the network, and the correspondence between key points should be known. However, existing public latent fingerprint databases usually have only two fingerprints for one finger. That is to say, one key point at most have two patches. In addition, to obtain the key point correspondences, additional key point matching is required, which would make the data preparation more complex and cannot guarantee the accuracy and completeness of correspondences.

To obtain large latent fingerprint database, an efficient alternative is to simulate fingerprint images. We therefore propose a fingerprint simulation method to efficiently obtain more reliable training data. Using this method, multiple image patches from the same key point can be obtained simultaneously. The basic idea is that, the transformation rule is analyzed in advance and then transferred to other fingerprints to simulate more images.

In the following, we first introduce the proposed fingerprint simulation method and then the generation of key point patches.

Fingerprint Simulation The simulation process includes two steps: learning transformation rule and simulating fingerprints from rolled fingerprints with the transformation rule. One example of the detailed steps is shown in Figure 8.

In the first step, we register latent fingerprints with corresponding rolled fingerprints to obtain the ROI and distortion field. The ROI is used to simulate small valid area of fingerprints while the distortion field is used to simulate the deformation.

We register two fingerprints in a similar manner with that in the data simulation of the proposed local patch alignment algorithm. The registration is conducted by fitting the TPS model with matched minutiae, which are found by spectral clustering method with similarities of minutiae pairs computed by MCC descriptor. After registering latent fingerprints to
rolled fingerprints, the intersection of the ROI of registered latent fingerprints and that of rolled fingerprints is seen as the common ROI. To better locate the relative position of the common ROI, the fingerprint center of the rolled fingerprint is also estimated. It is defined as the upper core of a fingerprint, which can be estimated by the VeriFinger [34]. It should be noted that we use the MCC-based minutiae matching algorithm to efficiently get pairs of training samples. Although the algorithm is not perfect, our experimental results show that the performance of the deep minutiae descriptor trained based on these training samples is significantly better than that of MCC.

In the second step, given one rolled fingerprint, a corresponding fingerprint can be simulated with the given distortion field and ROI. The ROI is firstly applied to the rolled fingerprint to cut a local fingerprint area. To ensure the right absolute position, the center recorded with ROI should be in advance aligned with the center of the rolled fingerprint. Then we apply the distortion field on the clipped local fingerprints. Finally, we apply the CycleGAN [35] to change the fingerprint appearance to simulate the gray-scale ridge pattern in various fingerprints. Multiple pairs of registered latent and rolled fingerprints are applied to train the model. In this way, the incompleteness, distortion, and different appearance of fingerprints are all simulated.

**Generation of Key Point Patches** By adopting the proposed fingerprint simulation method, twenty more fingerprints are simulated from a rolled fingerprint, such that more expressions are available for each fingerprint. After that, key point patches are generated to train the descriptor network.

We construct two training datasets to train the descriptors where image patches are centered on different key points. In the minutiae based dataset, image patches are centered on each minutia, and the minutiae orientation is used as the positive direction of the $x$ axis. In the sampling point based dataset, image patches are centered on each sampling point. The minutiae based dataset is used to train a base model since it is easy to get more accurate minutiae correspondences between fingerprints based on minutiae based registration methods. The sampling point based dataset is further applied to fine-tune the base model in order to make the model more generalizable to test data.

In both training datasets, the generation of images patches is the same. We take the minutiae based dataset as an example. For original rolled and latent fingerprints, as described earlier, minutiae are extracted from original fingerprint images, and minutiae pairs have been obtained from the registration result. For the simulated fingerprints, minutiae are estimated from that in rolled fingerprints with the distortion field, and the correspondences between minutiae in different impressions can be obtained directly. We cut minutiae patches of $160 \times 160$ pixels around each minutia in the rolled, latent, and simulated fingerprints separately for the minutiae descriptor training. Patches whose foreground area is less than 40% of the patch

![Empirical cumulative distribution functions of location (a) and direction (b) deviations on all the 258 pairs of fingerprints in NIST27 dataset.](image-url)

**Fig. 9.** Empirical cumulative distribution functions of location (a) and direction (b) deviations on all the 258 pairs of fingerprints in NIST27 dataset.
area area excluded. Based on the correspondences of minutiae from different impressions, the minutiae patches representing the same minutia share the same label. To ensure the correctness of each minutiae cluster, only minutiae clusters with more than eight patches are used to train minutiae descriptors.

The above patch generation algorithm can ensure that the image patches with the same label come from the same key point. To train the Siamese network, we select a mini-batch which is composed of several positive pairs. These pairs with the same label make up of the positive set, and negative set is sampled randomly from different categories.

D. Global Patch Matching

After obtaining the spatial transformation parameters and similarities between all pairs of sampling points, we first select the pairs whose similarity is above a given threshold \( \tau \) as potential sampling point correspondences, and then use the spectral clustering based global patch matching method to compute the compatible subset of correspondences.

Different from the spectral clustering based registration in minutiae based approaches [30], not only similarities but also the relative transformation parameters between pairs of sampling points are used in our method. For one pair of sampling points, we adjust the location and direction of sampling point on the latent fingerprint based on the estimated transformation. In this way, for different sampling points on the rolling fingerprint, the position and direction of the same point on the latent fingerprint are different after adjustment.

With the adjusted sampling point, the following registration is the same with that in minutiae based approaches. Specially, in consideration of time efficiency and accuracy, we choose mutually \( N \) neighbors from all pairs of adjusted sampling points as initial correspondences based on their similarities. The descriptor similarities are normalized by min-max normalization. In the following, the second-order graph matching [27] is applied to remove false correspondences.

E. Implementation Details

A database from local police department is used to construct the training data in both local patch alignment and matching procedures. This dataset contains more than one thousand pairs of rolled and latent fingerprints, where latent fingerprints are collected from real crime scenes.

We choose 500 pairs of mated latent and rolled fingerprints in the database and exclude those whose minutia matching scores computed by VeriFinger [34] are less than 50. Fingerprints of relatively good quality were chosen so that the data simulation results for training deep neural networks are reliable. FingerNet [3] is adopted to extract the ROI, minutiae, and ridge orientation images of both rolled and latent fingerprints.

All the networks in our method are trained with PyTorch [36] from scratch on NVIDIA GTX 1080 Ti GPUs. The stochastic gradient descent (SGD) is used for optimization with a weight decay of \( 5 \times 10^{-4} \).

To balance the loss function, we use \( \lambda_{\text{match}} = 0.25 \), and \( \lambda_{\text{simi}} = 0.5 \).

Local Patch Alignment We train two alignment models with different synthetic training datasets for two registration stages, both with learning rate \( 10^{-3} \), weight decay 0.95 every
9 epochs, and batch size of 32. Models are all trained for over 20 epochs.

**Local Patch Matching** The descriptor network is trained with the mini-batch which contains multiple pairs of patches with the same label, and on-line hard negative sampling is used to select the negative pairs with smallest distance during training for better convergence and accuracy.

When training the base model, the learning rate is set initially as $10^{-2}$ and decays at 0.95 rate every 5 epochs. The batch size is set as 32, and the model is trained for over 20 epochs. When fine-tuning the model with sampling point based training data, we use the initial learning rate $10^{-4}$, and other parameters are the same.

**Global Patch Matching** In coarse registration stage, we choose mutually $N = 6$ neighbors as initial matching pairs, and the threshold $\tau = 0.5$ to exclude obvious dissimilar point pairs. In precise registration, $N$ is set as 2, and $\tau$ is set as 0.

**IV. EXPERIMENTS**

In this section, we evaluate the performance of the proposed latent fingerprint registration algorithm and compare it to the state-of-the-art. The experiments are performed on the NIST27 database [6] and MOLF database [9]. The proposed deep descriptor, a key component of the whole system, is also evaluated on the NIST27 database.

**A. Performance of Fingerprint Registration on NIST27 database**

The NIST27 database [6] is a public latent fingerprint database containing 258 pairs of latent and rolled fingerprints. For a fingerprint image in the database, we do not conduct the preprocessing but request the ROI to define the sampling area of sampling points. We use manually marked ROI of latent fingerprints [27] and use FingerNet [3] to obtain the ROI of rolled ones. In order to guarantee the fairness, the same ROI is applied to all algorithms to be compared.

**Evaluation protocol** To evaluate the performance of the proposed fingerprint registration method, we use the location and direction differences of ground truth matching minutiae after alignment as the evaluation metric. In the NIST27 database, each pair of mated rolled and latent fingerprints has matching minutiae provided by fingerprint experts. If two fingerprints are aligned accurately, the location and direction differences between paired minutiae must be as small as possible.

After obtaining sampling point correspondences, the translation and rotation between image pairs are computed by the average translation and rotation between sampling point pairs. With the spatial transformation parameters, latent fingerprints can be aligned to rolled ones, and the manually marked minutiae on latent fingerprints can also be registered to evaluate the alignment performance.

We compare our method with Cao’s method in [8], which shows great performance on latent fingerprint recognition. They constructed three different minutiae templates and one
A subset as the reference dataset, which is captured texture template, and outputted one fingerprint registration result for each template. Therefore, the comparison is conducted with these four registration results.

**Results** The cumulative distribution functions of location and direction deviations are shown in Fig. [9] As we can see

- The performance of the proposed precise registration method is more accurate than that of coarse registration. After the precise registration, more than 85% minutiae have the deviation less than 20 pixels in location and 15 degrees in direction.
- The first minutiae template in [8] achieves better results than other two minutiae templates, and the performance of texture template is slightly better. Compared with these four templates, the performance of our method is consistently better.

For concrete analysis, we compare the performance on three subsets of NIST27 database, which are named as good, bad, and ugly subsets. The comparison results are shown in Fig. [10] Besides, to better analyze the results, we list the registration accuracy of different methods on three subsets and the whole dataset in Table [1] when setting the threshold of deviation from ground truth as 20 pixels and 15 degrees in location and direction, respectively. We can observe that

- The proposed method achieves comparable results on the good subset and performs better on the bad and ugly subset. As shown in the table, our method can achieve 4.43%, 6.89%, and 14.77% improvement in location in the good, bad, and ugly subset, 3.86% and 3.86% improvement in direction in the bad and ugly subset, respectively, in comparison with the best results in [8]. The improvement is greater when the image quality is worse, which suggests the superiority of the proposed method on latent fingerprints with low image quality.
- Among the four templates used in [8], the texture template performs better on bad and ugly subset than three minutiae templates. Its superior performance indicates that dense sampling points are suitable key points in latent fingerprints of very poor quality.

**Qualitative examples** We show several examples of correct matches and failure cases to discuss the superiority and inferiority of the proposed approach. Fig. [11] illustrates several examples where correct matches can be found by the proposed method, but the method in [8] is not successful. From these examples, it is demonstrated that the proposed method is robust in situations where fingerprint ridges are too deep or too light to distinguish from background or are polluted by background noise. Fig. [12] gives three failure cases, where registration error of the first example is large while the left two are close to correct matches. Here shows the sampling point correspondences obtained by coarse registration since precise registration is conducted for further reducing errors after basically correct registration. The failure is mostly due to limited fingerprint area and lack of discriminatory information. When the distances between matching points are too far after coarse registration, the effect of precise registration is limited. These examples show that the proposed method needs further improvement to deal with fingerprints with very small effective area or with very poor quality.

**B. Performance of Fingerprint Registration on MOLF database**

The MOLF database [9] contains 19,200 fingerprints from 100 subjects with five different capture methods. We choose the DB3_A subset as the reference dataset, which is captured using CrossMatch L-Scan Patrol, and the DB4 subset, which is the only latent fingerprint dataset. For each fingerprint, the first instance is selected. Finally, 1,000 pairs of latent and plain fingerprints from 10 fingers of 100 users are applied to conduct the experiments.

Considering the clean fingerprint background in these two datasets, the Otsu’s method [38] and morphological operations are used to obtain the ROI of each fingerprint. All the methods to be compared use the same ROI for fair comparison.

**Evaluation protocol** Because there are no marked minutiae pairs in the dataset, it is difficult to quantitatively evaluate the registration algorithms individually. We compute the discrepancy of rotation and translation parameters estimated by different registration methods to evaluate each method. When the parameters estimated by two algorithms are quite different, the registration performance is further judged manually. In this way, we can evaluate the relative performance of two registration methods.

To measure the discrepancy of different registration parameters, we compute the difference of imaginary grid of points deformed with each registration parameter. Concretely, for a latent fingerprint, we construct a grid of points with 40 pixels as interval, and transform them with estimated rotation and translation parameter. The average squared distances between two transformed grid points are taken as the discrepancy. If the average distance is less than 40, the two registration results are considered to be similar.

When judging the registration performance manually, the registration result are evaluated by scores in the range of 1 to 5. The closer the registration result is to the ground truth, the higher the score is. The scores of two registration results can be
the same when they are similar. When the registration results are completely wrong, it is defined as ERROR. In addition, when the method cannot produce the registration results, it is defined as FAIL.

**Result** Among the 1,000 pairs of fingerprints in the MOLF database, 75 pairs of fingerprints are found to be not corresponding fingerprints and thus should be excluded. 204 pairs of fingerprints are very hard samples for all algorithms and we cannot manually align them confidently.

For the remaining 721 pairs of fingerprints, the comparison result judged by the discrepancy of different registration parameters and manually is shown in Fig. 13. The image ID of these fingerprints and the results of all methods on them have been made public. As expected, the virtual minutiae based method performs much better than minutiae based methods on latent fingerprints. The proposed approach performs better than all four results in [8] since it obtains more score 5.

Fig. 14 gives two examples where our method conducts the registration successfully. Only the registration results by the texture template in [8] is shown for comparison since the minutiae templates often fails. The ridge lines in these latent fingerprints are difficult to be accurately extracted by existing algorithms but can be identified by human experts based on context information. The proposed method do not rely on estimated orientation field, and thus can handle such level of image blurriness. Fig. 15 shows two examples where the proposed approach fails. The failure mainly due to wrong estimation of rotation angle. In our method, the maximum rotation angle between two patches that can be estimated is 40 degrees, so it is not designed to deal with the situation that the rotation angle between a pair of fingerprints is very large. It is not a serious problem in practice since fingerprint examiners usually adjust latent fingerprints to upright direction.

**C. Effect of Coarse-to-Fine Registration**

Several examples are given to show the effect of precise registration in Fig. 16. In coarse registration, the intervals between sampling points are set very large to reduce the matching times of image patches in consideration of time efficiency. Therefore, the registered latent fingerprint is close to the correct result, but there is still a certain distance. To further reduce the registration error, the sampling points are denser in the precise matching. Despite of more sampling points, the matching times are acceptable since each sampling point in latent fingerprint is only compared with 25 sampling points in rolled ones. The registration results illustrates the effectiveness of precise registration.

**D. Computational Efficiency**

We compare the computational efficiency of proposed fingerprint registration method with [8]. The comparison is conducted detailed from three steps. The image preprocessing step consists of ROI estimation, ridge orientation estimation, fingerprint enhancement, and minutiae extraction. Our method only requires ROI of rolled fingerprints, which is estimated...
by the FingerNet. The descriptor extraction step is applied for each key point patch, and the operations in the two methods are different. In \cite{8}, they extract deep descriptors from each key point patch on latent and rolled fingerprints, respectively, followed by descriptor length reduction and product quantization to improve the comparison speed. In our method, this step adjusts the location and direction of sampling points with estimated transformation parameter and extracts the deep descriptors from two image patches simultaneously. In the key point matching step, similarities between key points are computed, and global patch matching approach is applied in both methods to conduct the fingerprint comparison. The time taken for each step is shown in Table \ref{tab:2}.

All the steps that require deep learning are conducted on NVIDIA GTX 1080 Ti. The key point matching in \cite{8} is implemented with C++ while ours are implemented in MATLAB on a PC with 2.50 GHz CPU.

From Table \ref{tab:2}, the method in \cite{8} takes a lot of time in the image preprocessing and extracting deep descriptors of latent fingerprints, average 32.91 seconds and 137.48 seconds for one latent fingerprint, respectively. This is mainly due to the need of obtaining four enhanced images, seven minutiae sets, and one virtual minutiae set, and extracting 28 minutiae templates and one texture template. Among the three operations in the descriptor extraction step, the most time-consuming is descriptor length reduction, for which more than two minutes are required. But in practice, they select finally three minutiae templates, and thus the computation time can be shortened. Besides, they extract minutiae templates for each input fingerprint separately. Once minutiae templates are obtained, they can conduct matching between any pair of fingerprints efficiently.

Compared with the method in \cite{8}, ours skips image preprocessing, but requires longer time when registering a pair of fingerprints due to the two-stage registration. It takes more than one minutes for one pair of fingerprints. In addition, when matching each pair of input fingerprints, the descriptor extraction is required. Therefore, the proposed method is more suitable for performing fine registration in the candidate lists generated by large database retrieval.

| Method               | Cao and Jain \cite{8} | Ours-coarse | Ours-precise |
|----------------------|-----------------------|-------------|--------------|
| Image preprocessing  | 32.91                 | 1.17        | 0.21         |
| Desciptor extraction | 137.48 (15.49+121.96+0.03) | 19.39 (10.23+9.13+0.03) | 27.41 | 34.03 |
| Key point matching   | 0.001                 | 2.933       | 3.903        |

V. CONCLUSION

In this paper, we propose a latent fingerprint registration method, which bypasses minutiae extraction and ridge orientation field estimation to avoid being affected by the error of feature extraction. Instead of minutiae, dense undirected sampling points are taken as the key points. All pairs of sampling points are compared to produce their similarities along with their relative spatial transformation. The sampling point correspondences are finally estimated by spectral clustering based global patch matching method. To further reduce the registration error while not sacrificing efficiency, an coarse-to-fine registration scheme is conducted. The proposed latent fingerprint registration algorithm is tested on NIST27 database and MOLF database and compared with the state-of-the-art. Experimental results show its better performance on latent fingerprints and stronger ability to handle fingerprints with poor quality.

The limitation of the proposed approach is that (1) although the coarse-to-fine registration scheme helps increase the efficiency, the local patch alignment and matching itself is time-consuming. (2) It is inevitably affected by large skin distortion due to the performance constraints of local patch alignment and matching. (3) There is still room for improvement in the discrimination ability of the proposed deep key point descriptor.

Further direction includes increasing the computational efficiency while increasing the registration accuracy to better deal with local distortion, and achieving end-to-end fingerprint registration.

REFERENCES

[1] Davide Maltoni, Dario Maio, Anil K Jain, and Salil Prabhakar. Handbook of Fingerprint Recognition. Springer Science & Business Media, 2009.
[2] Anush Sankaran, Mayank Vatsa, and Richa Singh. Latent fingerprint matching: A survey. *IEEE Access*, 2:982–1004, 2014.
[3] Yao Tang, Fei Gao, Jufu Feng, and Yuhang Liu. FingerNet: An unified deep network for fingerprint minutiae extraction. In *Biometrics (IJCB), 2017 IEEE International Joint Conference on*, pages 108–116. IEEE, 2017.
[4] Asker M Bazen and Sabih H Gerez. Fingerprint matching by thin-plate spline modelling of elastic deformations. *Pattern Recognition*, 36(8):1859–1867, 2003.
[5] Arun Ross, Sarat Dass, and Anil Jain. A deformable model for fingerprint matching. *Pattern Recognition*, 38(1):95–103, 2005.
[6] NIST Special Database 27. [http://www.nist.gov/srd/nistsd27.cfm](http://www.nist.gov/srd/nistsd27.cfm).
[7] Kai Cao and Anil K Jain. Automated latent fingerprint recognition. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 41(4):788–800, 2019.
[8] Kai Cao, Dinh-Luan Nguyen, Cori Tymoszek, and Anil K Jain. End-to-end latent fingerprint search. *IEEE Transactions on Information Forensics and Security*, 15:880–894, 2020.
[9] Anush Sankaran, Mayank Vatsa, and Richa Singh. Multisensor optical and latent fingerprint database. *IEEE Access*, 3:653–665, 2015.
[10] Arun Ross, Sarat C Dass, and Anil K Jain. Fingerprint warping using ridge curve correspondences. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 28(1):19–30, 2005.

[11] Chenhao Lin and Ajay Kumar. Matching contactless and contact-based conventional fingerprint images for biometrics identification. *IEEE Transactions on Image Processing*, 27(4):2008–2021, 2018.

[12] Xuanbin Si, Jianjiang Feng, Bo Yuan, and Jie Zhou. Dense registration of fingerprints. *Pattern Recognition*, 63:87–101, 2017.

[13] Zhe Cui, Jianjiang Feng, Shihao Li, Jiwen Lu, and Jie Zhou. 2-d phase demodulation for deformable fingerprint registration. *IEEE Transactions on Information Forensics and Security*, 13(12):3153–3165, 2018.

[14] Anil K Jain, Yi Chen, and Meltem Demirkus. Pores and ridges: High-resolution fingerprint matching using level 3 features. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 29(1):15–27, 2006.

[15] Zsolt Miklos Kovacs-Vajna. A fingerprint verification system based on triangular matching and dynamic time warping. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 22(1):1266–1276, 2000.

[16] Asker M Bazen, Gerben TB Verwaaijen, Sabih H Gerez, Leo PJ Veelenturf, and Berend Jan Van Der Zwaag. A correlation-based fingerprint verification system. In *Proceedings of the Pro-KISC2000 Workshop on Circuits, Systems and Signal Processing*, 2000.

[17] Marius Tico and Pauli Kuosmanen. Fingerprint matching using an orientation-based minutia descriptor. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 25(8):1009–1014, 2003.

[18] Farid Bennhamadi, MN Amirouche, Hamid Hentous, K Bey Bechdadj, and Mohamed Aissani. Fingerprint matching from minutiae texture maps. *Pattern Recognition*, 40(1):189–197, 2007.

[19] Xinjian Chen, Jie Tian, and Xin Yang. A new algorithm for distorted fingerprints matching based on normalized fuzzy similarity measure. *IEEE Transactions on Image Processing*, 15(3):767–776, 2006.

[20] Jianjiang Feng. Combining minutiae descriptors for fingerprint matching. *Pattern Recognition*, 41(1):342–352, 2008.

[21] Raffaele Cappelli, Matteo Ferrara, and Davide Maltoni. Minutia cylinder-code: A new representation and matching technique for fingerprint recognition. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 32(12):2128–2141, 2010.

[22] Ogechukwu Iloanusi, Aglika Gyaourova, and Arun Ross. Indexing fingerprints using minutiae quadruplets. In *Computer Vision and Pattern Recognition Workshops (CVPRW), 2011 IEEE Computer Society Conference on*, pages 127–133. IEEE, 2011.

[23] Javad Khodadoust and Ali Mohammad Khodadoust. Fingerprint indexing based on minutiae pairs and convex core point. *Pattern Recognition*, 67:110–126, 2017.

[24] Guoqiang Li, Bian Yang, and Christoph Busch. A score-level fusion fingerprint indexing approach based on minutiae vicinity and minutia cylinder-code. In *Biometrics and Forensics (IWBF), 2014 International Workshop on*, pages 1–6. IEEE, 2014.

[25] Fandong Zhang, Shiyuan Xin, and Jufu Feng. Combining global and minutia deep features for partial high-resolution fingerprint matching. *Pattern Recognition Letters*, 2017.

[26] Dehua Song, Yao Tang, and Jufu Feng. Aggregating minutia-centred deep convolutional features for fingerprint indexing. *Pattern Recognition*, 88:397–408, 2019.

[27] Xiang Fu, Chongjin Liu, Junjie Bian, Jufu Feng, Han Wang, and Zhiwei Mao. Extended clique models: A new matching strategy for fingerprint recognition. In *2013 International Conference on Biometrics (ICB)*, pages 1–6. IEEE, 2013.

[28] Xiang Fu and Jufu Feng. Minutia tensor matrix: A new strategy for fingerprint matching. *PloS one*, 10(3):e0118910, 2015.

[29] Ignacio Rocco, Relja Arandjelovic, and Josef Sivic. Convolutional neural network architecture for geometric matching. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pages 6148–6157, 2017.

[30] Marius Leordeanu and Martial Hebert. A spectral technique for correspondence problems using pairwise constraints. In *ICCV*, 2005.

[31] Fred L. Bookstein. Principal warps: Thin-plate splines and the decomposition of deformations. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 11(6):567–585, 1989.

[32] Bertram Düring, Carsten Gottschlich, Stephan Huckemann, Lisa Maria Kreusser, and Carola-Bibiane Schönlieb. An anisotropic interaction model for simulating fingerprints. *Journal of Mathematical Biology*, 78(7):2171–2206, 2019.

[33] Kai Cao and Anil Jain. Fingerprint synthesis: Evaluating fingerprint search at scale. In *2018 International Conference on Biometrics (ICB)*, pages 31–38. IEEE, 2018.

[34] Neurotechnology Inc., VeriFinger. [http://www.neurotechnology.com](http://www.neurotechnology.com).

[35] Jun-Yan Zhu, Taesung Park, Phillip Isola, and Alexei A Efros. Unpaired image-to-image translation using cycle-consistent adversarial networks. In *Proceedings of the IEEE International Conference on Computer Vision*, pages 2223–2232, 2017.

[36] Adam Paszke, Sam Gross, Soumith Chintala, Gregory Chanan, Edward Yang, Zachary DeVito, Zeming Lin, Alban Desmaison, Luca Antiga, and Adam Lerer. Automatic differentiation in pytorch. In *NIPS-W*, 2017.

[37] Soweon Yoon, Jianjiang Feng, and Anil K Jain. Latent fingerprint enhancement via robust orientation field estimation. In *2011 International Joint Conference on Biometrics (IJCB)*, pages 1–8. IEEE, 2011.

[38] Nobuyuki Otsu. A threshold selection method from gray-level histograms. *IEEE Transactions on Systems, Man, and Cybernetics*, 9(1):62–66, 1979.