Phase transition in an $O(N)$ gauge model in two dimensions

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We study the phase transition properties of the nonlinear $O(N)$ $\sigma$ model in two dimensions when $O(N)$ gauge interactions are included. With nonzero gauge coupling, this theory exhibits a first-order phase transition in the large-$N$ limit. The broken-symmetry phase is stabilized by the Higgs mechanism and Goldstone bosons do not appear.

Recently, Bardeen and Pearson\textsuperscript{1} have proposed a transverse-lattice formulation of quantum chromodynamics.\textsuperscript{2} In this theory, color confinement is obtained when the vacuum is invariant under the transverse gauge symmetry. A quark-gluon phase, where color is not confined, can result if this symmetry is spontaneously broken. In this paper we will study some aspects of the mechanisms which are responsible for generating such a phase transition.

The independent gauge degrees of freedom or the transverse-lattice theory are associated with links on the transverse lattice. The longitudinal dynamics of a single transverse link consists of a nonlinear SU(3)$\times$SU(3) $\sigma$ model with SU(3)$\times$SU(3) gauge interactions. For a single transverse link the longitudinal dynamics is two-dimensional. As the transverse gauge symmetry is a local symmetry on the lattice, the phase-transition properties of a single transverse link are relevant to the phase-transition properties of the full gauge theory.

We shall study a somewhat simpler though analogous version of the single-link problem. The model consists of a two-dimensional nonlinear $O(N)$ $\sigma$ model with $O(N)$ gauge interactions. This theory has the advantage that the model may be systematically studied in the large-$N$ limit. The nonlinear $\sigma$ model in 2 and $2+\epsilon$ dimensions has recently been extensively studied by Brezin and Zinn-Justin\textsuperscript{3} and by Bardeen, Lee, and Shrock.\textsuperscript{4} In this theory, spontaneous symmetry breaking can occur in $2+\epsilon$ dimensions but only the symmetric phase can exist in 2 dimensions. The basic result of our paper is that the broken-symmetry phase can be stabilized when gauge interactions are introduced. The existence of nontrivial phase-transition properties in two dimensions makes this theory interesting in its own right.

The nonlinear $O(N)$ $\sigma$ model with gauge interactions is described by the Lagrangian

$$L = \frac{1}{2} (D_\mu \vec{\phi})^2 - \frac{1}{4} (G_{\mu\nu})^2,$$

where $\vec{\phi}$ is an $N$-component scalar field with the constraint $\vec{\phi}^2 = f_0^2$. The gauge fields may be written as an antisymmetric tensor $(A_{\mu ij}, i, j = 1, \ldots, N)$. The covariant derivative is defined by

$$\langle D_\mu \phi \rangle_i = \partial_\mu \phi_i + g A_{\mu ij} \phi_j$$

and the Yang-Mills field strength is given by

$$G_{\mu ij} = \partial_\mu A_{ij} - \partial_i A_{\mu j} + g A_{\mu kl} A_{ijkl} + g A_{\mu jk} A_{ikl}.$$}

In two dimensions this theory is renormalizable with respect to the dimensionless coupling constant $1/f_0^2$, and super-renormalizable with respect to the gauge coupling constant $g^2$.

This theory may be studied directly using the methods discussed in Ref. 4. Since the nonlinear theory is renormalizable, we must be careful to preserve the symmetry structure of the theory in our calculation. Dimensional regularization is not particularly convenient in this case as we would confront the necessity of including contributions from the transverse gauge fields. Instead, we choose to regularize the theory by considering the linear $\sigma$ model in precisely two dimensions. The nonlinear theory is recovered as a limit of the linear theory.\textsuperscript{5}

The linearized theory is described by the Lagrangian

$$L = \frac{1}{2} (D_\mu \vec{\phi})^2 - \frac{1}{4} \lambda_0 (f_0^2 - \vec{\phi}^2)^2 - \frac{1}{4} (G_{\mu\nu})^2,$$

where the constraint $\vec{\phi}^2 = f_0^2$ has been relaxed. The nonlinear model is obtained by taking the limit $\lambda_0 \rightarrow \infty$ with $f_0^2$ and $g^2$ fixed. Since the nonlinear theory is renormalizable, only a logarithmic dependence on $\lambda_0$ can occur and is absorbed by the renormalization of $f_0^2$. In the large-$N$ limit no such logarithms appear and the limit may be taken without the renormalization involving $\lambda_0$.\textsuperscript{6}
The theory is most easily studied in the light-cone gauge, $A_{\pm} = 0$, $A_{\pm} = (1/\sqrt{2})(A_\pm + A_\mp)$. The gauge fields $A_{\pm}$ are dependent and may be eliminated in favor of a "Coulomb" interaction. In this gauge, the Lagrangian of Eq. (4) becomes

$$\mathcal{L} = \frac{1}{2} (\partial_{\mu} \phi)^2 - \frac{1}{2} \lambda_0 (f_0^2 - \phi^2)^2 - 4g^2 \langle \phi \partial_{\mu} \phi \rangle (\partial_{\mu} \phi)^2 - \frac{1}{2} g^2 \langle \phi \partial_{\mu} \phi \rangle (\partial_{\mu} \phi)^2,$$

(5)

where

$$\partial_{\pm} = \frac{1}{\sqrt{2}} (\partial_\tau \pm \partial_\sigma).$$

We wish to consider the possibility of spontaneous symmetry breaking of the $O(N)$ symmetry where the field, $\phi$, acquires a nonzero vacuum expectation value. The direction of the symmetry breaking may be rotated to any fixed axis. There remains an $O(N-1)$ symmetry. We rewrite the field, $\phi$, as a field, $\sigma$, which can have a vacuum expectation value, and fields $\pi_i$, $i = 1, \ldots, (N-1)$ which have zero vacuum expectation value. We may probe the broken phase by adding a Lagrange multiplier, $J$, to force the $\sigma$ field to have a given expectation value, $f$. A spontaneously broken symmetry phase exists if $f \neq 0$ for $J = 0$ and if this phase has the lowest vacuum energy. The Lagrangian of Eq. (5) may be rewritten as

$$\mathcal{L} = \frac{1}{2} (\sigma \partial_\mu \sigma)^2 + \frac{1}{2} |(\partial_\mu \pi)|^2 - 3 \lambda_0 (f_0^2 - \sigma^2 - \pi^2)^2 + J (\sigma - f)$$

$$- \frac{1}{2} g^2 (\partial_{\mu} \pi) (\partial_{\mu} \pi) - \frac{1}{2} g^2 (\partial_{\mu} \pi) (\partial_{\mu} \pi),$$

(6)

(a) $\langle \sigma \rangle_0 = f,$
(b) $\langle \pi \rangle_0 = 0,$
(c) $\langle \sigma^2 \rangle_0 = \langle \sigma \rangle^2 + \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\sigma^2)^{-1} = f^2 + (4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2},$
(d) $\langle \pi^2 \rangle_0 = (N-1) \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\pi^2)^{-1} = (N-1)(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2},$
(e) $\langle (\partial_\mu \sigma)(\partial_{\mu} \sigma)^{-1}(\partial_\mu \pi) \rangle_0 = - \langle \sigma \rangle^2 - \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\sigma^2)^{-1} (k_+ + P_\pi^2) (k_- - P_-)^{-2}$

$$= - f^2 - \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\sigma^2)^{-1} - \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\pi^2)^{-1} \frac{2k_+ 2P_-}{(k_- - P_-)^2}$$

$$= - f^2 - (4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2} + \frac{1}{\pi},$$

(f) $\sum_i \langle (\partial_\mu \pi)(\partial_{\mu} \pi)^{-1}(\partial_\mu \pi) \rangle_0 = - (N-1) \frac{i}{(2\pi)^2} \int d^2 k (k^2 - m_\pi^2)^{-1} (k_+ + P_\pi^2) (k_- - P_-)^{-2} = (N-1)(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2} + (N-1) \frac{1}{\pi},$
(g) $\langle \sigma^3 \rangle_0 = f^3 + 3f(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2},$
(h) $\langle \sigma^2 \pi \rangle_0 = f(N-1)(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2}$,
(i) $\sum_i \langle (\partial_\mu \pi)(\partial_{\mu} \pi)^{-1}(\partial_\mu \pi) \rangle = f \left( - (N-1)(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2} + (N-1) \frac{1}{\pi} \right).$
The divergent self-energy integrals have been computed using a Wick rotation and a cutoff, \( \Lambda^2 \).

Using the results of Eq. (10), we may compute all the large-\( N \) contributions to Eqs. (7), (8), and (9). The propagators are given by

\[
\begin{align*}
\Gamma^{(2)}_{\alpha}(p^2) &= P^2 - m^2_{\alpha}, \\
\Gamma^{(2)}_{\pi}(p^2) &= P^2 - m^2_{\pi},
\end{align*}
\]

where

\[
\begin{align*}
m^2_{\alpha} &= -\lambda_{\alpha} f^2 + 3\lambda_{\alpha} f^2 + \lambda_{\alpha} N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} \\
&\quad + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} - \frac{g^2 N}{\pi},
\end{align*}
\]

\[
\begin{align*}
m^2_{\pi} &= -\lambda_{\alpha} f^2 + \lambda_{\alpha} f^2 + \lambda_{\alpha} N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} \\
&\quad + g^2 f^2 + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} - \frac{g^2 N}{\pi}.
\end{align*}
\]

The Lagrange multiplier is determined by the equation

\[
J = -\lambda_{\alpha} f^2 + \lambda_{\alpha} f^2 + \lambda_{\alpha} N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} \\
+ g^2 f^2 + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} - \frac{g^2 N}{\pi}
\]

\[
= f (m^2_{\pi} - g^2 f^2). \tag{12}
\]

The Hartree calculation sums consistently in leading order \( N \), all tadpole graphs [Fig. 1(a)], all cactus graphs [Fig. 1(b)], and all rainbow graphs [Fig. 1(c)]. All other graphs are nonleading in the large-\( N \) limit.

The \( \pi \) mass, \( m^2_{\pi} \), must be determined self-consistently from Eq. (11) and Eq. (12). In the case \( J = 0 \), there are two possible solutions corresponding to the symmetric phase, \( f = 0 \), and a spontaneously broken phase, \( f \neq 0 \). In the symmetric phase we have \( f = 0 \),

\[
\begin{align*}
m^2_{\pi} &= -\lambda_{\alpha} f^2 + \lambda_{\alpha} N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} \\
&\quad + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} - \frac{g^2 N}{\pi}.
\end{align*}
\]

In the broken-symmetry phase we have

\[
\begin{align*}
f^2 &= m^2_{\pi} / g^2, \\
-(\lambda_{\alpha} f^2) m^2_{\pi} &= -\lambda_{\alpha} f^2 + \lambda_{\alpha} N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} \\
&\quad + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m^2_{\pi}} - \frac{g^2 N}{\pi}.
\end{align*}
\]

Now we wish to compute the dependence of the vacuum energy density, \( V \), on the order parameter, \( f \). The vacuum energy may be computed from

\[
\exp \left( -i \int dx \, V \right) = \left( \exp \left( i \int dx \, \mathcal{L} \right) \right) \, \phi,
\]

where \( \mathcal{L} \) is the Lagrangian of Eq. (6). Instead of computing \( V \) directly, we shall evaluate \( \partial_f V \) using the result of Eq. (10). This ensures a systematic treatment of all divergences. We obtain

\[
- \partial_f V = - J + (\partial_f \phi)(\phi - f) \, \phi = - J. \tag{16}
\]

This expression may be integrated by considering a similar derivative of the mass equation for \( m^2_{\pi} \), Eq. (11). We obtain

\[
\left[ 1 + (\lambda_{\alpha} + g^2) \right] (m^2_{\pi})^{-1} \partial_f m^2_{\pi} = 2f(\lambda_{\alpha} + g^2). \tag{17}
\]

When Eqs. (16), (12), and (17) are combined, the derivative of the vacuum energy becomes

\[
\partial_f V = f (m^2_{\pi} - g^2 f^2)
\]

\[
= \frac{1}{2} [m^2_{\pi}(\lambda_{\alpha} + g^2)^{-1} + N(4\pi)^{-1}] \partial_f m^2_{\pi} - \frac{1}{2} g f^2 + V_0, \tag{18}
\]

Equation (18) may be directly integrated to yield the vacuum energy:

\[
V = \frac{1}{2} m^2_{\pi}(\lambda_{\alpha} + g^2)^{-1} + \frac{1}{2} N(4\pi)^{-1} m^2_{\pi} - \frac{1}{2} g f^2 + V_0, \tag{19}
\]

where \( V_0 \) can depend on \( \lambda_{\alpha} \), \( g^2 \), and \( f_0^2 \) but not on \( f \).
$$m_\sigma^2 = -\lambda_\sigma f_0^2 + 3\lambda_\sigma f^2 + \lambda_\sigma N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2}$$

$$+ g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2}$$

$$m_\pi^2 = -\lambda_\sigma f_0^2 + 3\lambda_\sigma f^2 + \lambda_\sigma N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2}$$

$$+ g^2 f^2 + g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2}$$

$$J = f(m_\sigma^2 - g^2 f^2),$$

$$V = \frac{1}{2} m_\sigma^4 (\lambda_\sigma + g^2)^{-1} + \frac{1}{2} N(4\pi)^{-1} m_\sigma^2 - \frac{1}{2} g^2 f^2.$$  (20)

The two distinct phases occur when $J = 0$. The symmetric phase is determined by

$$f = 0,$$

$$m_\sigma^2 = -\lambda_\sigma f_0^2 + \lambda_\sigma N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2}$$

$$+ g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\sigma^2}$$

$$m_\pi^2 = m_\pi^2,$$

$$V = \frac{1}{2} m_\pi^4 (\lambda_\sigma + g^2)^{-1} + \frac{1}{2} N(4\pi)^{-1} m_\pi^2.$$  (21)

The broken phase is determined by

$$f^2 = m_\pi^2 / h^2$$

$$- (\lambda_\sigma / g^2) m_\pi^2 = -\lambda_\sigma f_0^2 + \lambda_\sigma N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2}$$

$$+ g^2 N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2}$$

$$m_\sigma^2 = m_\pi^2$$

$$V = \frac{1}{2} m_\pi^4 (\lambda_\sigma + g^2)^{-1} + \frac{1}{2} N(4\pi)^{-1} m_\pi^2 - \frac{1}{4} m_\pi^4 / g^2.$$  (22)

Since we are using the linear $O(N)$ model to regularize the nonlinear $O(N)$ model, we will not discuss the linear theory but proceed to a discussion of the nonlinear theory. We note that all expressions we have used are unrenormalized. The only divergent renormalization necessary in the large-$N$ limit is a logarithmic divergence in $f_0^2$.

The nonlinear $O(N)$ gauge theory is obtained by taking the limit $\lambda_\sigma \to \infty$ with all other parameters held fixed. One might worry that such a limit might reorder the large-$N$ expansion. However, we have noted that in two dimensions the nonlinear theory is renormalizable with only logarithmic divergences. Hence, the large-$N$ limit cannot be modified by powers of $N$ and no reordering can occur.

The phase-transition properties of the nonlinear theory may be obtained by taking the nonlinear limit of Eq. (21) and Eq. (22). The symmetric phase is determined by

$$f = 0,$$

$$f_0^2 = N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2},$$

$$m_\sigma^2 = m_\pi^2,$$

$$V = \frac{1}{2} N(4\pi)^{-1} m_\pi^2.$$  (23)

The broken-symmetry phase is determined by

$$f^2 = m_\pi^2 / h^2$$

$$f_0^2 = m_\pi^2 + N(4\pi)^{-1} \ln \frac{\Lambda^2}{m_\pi^2},$$

$$m_\sigma^2 = \infty,$$

$$V = \frac{1}{2} N(4\pi)^{-1} m_\pi^2 - \frac{1}{4} m_\pi^4 / g^2.$$  (24)

In this phase the $\sigma$ is not formed as a bound state. Only the $O(N - 1)$ Coulomb interactions are operative with the remaining Coulomb interactions being screened. The physical states are $O(N - 1)$-singlet bound states of $\pi$ and the broken-symmetry phase avoids Coleman's theorem as the Higgs mechanism does not permit the existence of Goldstone bosons.

We must now discuss the stability of the two phases to see the range of couplings where each phase can exist and the character of the phase transition. We introduce a renormalized coupling constant, $h$, through the relation

$$\frac{N(4\pi)^{-1}}{h} = f_0^2 - N(4\pi)^{-1} \ln \frac{\Lambda^2}{M^2},$$

where $M^2$ is a normalization scale, and we define the fine-structure constant, $\alpha = g^2 N / 4\pi$. Equations (23) and (24) become the following.

(a) symmetric phase

$$\frac{1}{h} = \ln \frac{M^2}{m_\pi^2} \quad \text{or} \quad m_\pi^2 = M^2 e^{-1/\alpha},$$

$$V = \frac{1}{2} N(4\pi)^{-1} m_\pi^2.$$  (25)

(b) broken-symmetry phase

$$\frac{1}{h} = \frac{m_\pi^2}{\alpha} + \ln \frac{M^2}{m_\pi^2},$$

$$V = \frac{1}{2} N(4\pi)^{-1} (m_\pi^2 - \frac{1}{2} m_\pi^4 / \alpha).$$  (26)
The symmetric phase can exist for all values of the coupling constants. The broken-symmetry phase can exist only if the coupling constant, \( h \), is sufficiently small. Since the \( \sigma \)-model coupling constant is directly related to the mass in the symmetric phase, we consider the phase properties of the theory expressed in terms of this mass. We denote the \( \pi \) masses in the symmetric and broken phases by \( m_s^2 \) and \( m_b^2 \), respectively. As mentioned above we use \( m_s^2 \) to parametrize theory in both phases. In Fig. 2 we plot the \( \pi \) masses in each phase for different values of the fine-structure constant. In Fig. 3 we plot the vacuum energy for a fixed value of the fine-structure constant. In Fig. 4, we plot the phase-transition line in coupling-constant space.

By examining Fig. 2, we see that only the symmetric phase (I) can exist for \( m_s^2 > \alpha/e \). For \( m_s^2 < \alpha/e \), the broken-symmetry phase can also exist with two possible branches (II, III). As we decrease the gauge coupling constant \( (a-b-c) \), the region where the broken phase can exist is restricted to smaller values of \( m_s^2 \), or, equivalently, smaller values of the coupling constant \( h \). When the gauge coupling constant vanishes \(( \alpha = 0 )\), only the symmetric phase can exist, in agreement with the discussions of Ref. 3 and Ref. 4.

Although two broken-symmetry phases can exist for \( m_s^2 < \alpha/e = 0.368\alpha \), the phase transition does not occur until \( m_s^2 \leq 0.321\alpha \), as seen in Fig. 3. For small \( m_s^2 \) \(( \leq 0.321\alpha )\), the stable phase is the larger-mass broken-symmetry phase (III). The vacuum energy is, of course, continuous through the phase transition. However, both \( m_s^2 \) and \( f^2 \) are discontinuous, which indicates that it is a first-order phase transition. In Fig. 4 we plot the phase-transition line in coupling-constant space where region A is the symmetric phase and region B is the broken-symmetry phase.
In this paper we have studied the phase-transition properties of a nonlinear $O(N)$ $\sigma$ model with gauge interactions. When studied in the large-$N$ limit the theory exhibits a first-order phase transition. The symmetric phase is characterized by the generation of a bound-state $\sigma$ particle degenerate with the $\pi$'s and by all physical states being $O(N)$ singlet bound states of $\sigma$ and $\pi$'s. The broken-symmetry phase is characterized by a residual $O(N - 1)$ symmetry. The $\sigma$ bound states are not formed and all physical states are $O(N - 1)$ singlet bound states. The Higgs mechanism avoids the necessity of Goldstone bosons and stabilizes the broken-symmetry phase in two dimensions.

These results indicate that the longitudinal dynamics of the gluon fields in the transverse-lattice theory of Bardeen and Pearson\(^1\) is rich enough to support a phase transition in the quark-gluon theory, as would be expected in $4 + \epsilon$ dimensions or if the number of quarks were to be sufficiently large as to destabilize confinement phase. The phase-transition properties of the full gauge theory are of course much more complex than the simple model studied in this paper. We do think that the results of this paper shed some light on the mechanisms which operate in a gauge theory.

**Note added.** After this paper was completed, we received a report by J. S. Kang [Phys. Rev. D 14, 1587 (1976)], who studies the linear $O(N)$ gauge model. His calculations include the leading-$N$ contribution from the meson self-interaction but are to first order in the gauge coupling. Our results represent the full leading-$N$ calculation of the properties of the linear and nonlinear $O(N)$ gauge theories in two dimensions.

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\(^{a}\) Operated by Universities Research Association Inc. under contract with the Energy Research and Development Administration.

\(^{1}\) William A. Bardeen and Robert B. Pearson, Phys. Rev. D 14, 547 (1976).

\(^{2}\) Alternative lattice formulations of this theory have been proposed by K. Wilson [Phys. Rev. D 10, 2445 (1974)] and by J. Kogut and L. Susskind [ibid. 11, 399 (1975)].

\(^{3}\) E. Brezin and J. Zinn-Justin, Phys. Rev. Lett. 36, 691 (1976) and CEN Saclay report (unpublished); see also A. Polyakov, Phys. Lett. 59B, 79 (1975) and A. Migdal, Landau Institute Report, 1975 (unpublished).

\(^{4}\) W. A. Bardeen, B. W. Lee, and R. E. Shrock, Phys. Rev. D 14, 985 (1976).

\(^{5}\) Without gauge couplings, the linear model has been studied in the large-$N$ limit by S. Coleman, R. Jackiw, and H. D. Politzer [Phys. Rev. D 10, 2491 (1974)]; R. G. Root [ibid. 10, 3322 (1974)]; and L. F. Abbott et al. [ibid. 13, 2212 (1976)].

\(^{6}\) To establish this intuitive result rigorously, we would have to study a Bethe-Salpeter equation analogous to that proposed by G. 't Hooft [Nucl. Phys. B75, 461 (1964)] and further elaborated upon by C. G. Callan, N. Coote, and D. Gross [Phys. Rev. D 13, 1649 (1976)] and by M. E. Einhorn [Fermilab Report No. Fermilab-Pub-76/22-THY (unpublished)].

\(^{7}\) S. Coleman, Commun. Math. Phys. 31, 259 (1973).