VALES VII: Molecular and ionized gas properties in pressure balanced interstellar medium of starburst galaxies at $z \sim 0.15$. 

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ABSTRACT

Context. Spatially resolved observations of the ionized and molecular gas are critical for understanding the physical processes that govern the interstellar medium (ISM) in galaxies. The observation of starburst systems is also important as these present extreme gas conditions that may help to test different ISM models. However, matched resolution imaging at ~kpc scales for both ISM gas phases are usually scarce and the ISM properties of starbursts still remain poorly understood.

Aims. We aim to study the morpho-kinematic properties of the ionized and molecular gas in three dusty starburst galaxies at $z = 0.12$ – 0.17 to explore the relation between molecular ISM gas phase dynamics and the star-formation activity.

Methods. We employ two-dimensional dynamical modelling to analyse Atacama Large Millimeter/submillimeter Array (ALMA) CO(1–0) and seeing limited Spectrograph for INtegral Field Observations in the Near Infrared (SINFONI) Paschen-α (Paα) observations tracing the molecular and ionized gas morpho-kinematics at ~kpc-scales. We use a dynamical mass model, which accounts for beam-smearing effects, to constrain the CO-to-H$_2$ conversion factor and estimate the molecular gas mass content.

Results. One starburst galaxy shows irregular morphology which may indicate a major merger, while the other two systems show disc-like morpho-kinematics. The two disc-like starbursts show molecular gas velocity dispersion values comparable with that seen in local Luminous and Ultra Luminous Infrared Galaxies, but in an ISM with molecular gas fraction and surface density values in the range of the estimates reported for local star-forming galaxies. We find that these molecular gas velocity dispersion values can be explained by assuming vertical pressure equilibrium. We also find that the star-formation activity, traced by the Paα emission line, is well correlated with the molecular gas content suggesting an enhanced star formation efficiency and depletion times of the order of ~ 0.1 – 1 Gyr. We find that the star formation rate surface density ($\Sigma_{\text{SFR}}$) correlates with the ISM pressure set by self-gravity ($P_{\text{gas}}$) following a power law with an exponent close to 0.8.

Conclusions. In dusty disc-like starburst galaxies, our data support the scenario in which the molecular gas velocity dispersion values are driven by the ISM pressure set by self-gravity, responsible to maintain the vertical pressure balance. The correlation between $\Sigma_{\text{SFR}}$ and $P_{\text{gas}}$ suggests that, in these dusty starbursts galaxies, the star formation activity arises as a consequence of the ISM pressure balance.

Key words. galaxies: star formation – galaxies: starburst – ISM: kinematics and dynamics

1. Introduction

Understanding how galaxies build up their stellar mass content within dark matter haloes is a key goal in modern extragalactic astrophysics. One of the best constraints comes from studying the evolution of the star formation rate density (SFRD) across cosmic time (Madau et al. 1996; Madau & Dickinson 2014). The overall decline of the SFRD in the last ~10 Gyr coincides with the decrease of the average fraction of molecular gas mass in galaxies (Tacconi et al. 2010; Geach et al. 2012; Carilli & Walter 2013). A straightforward interpretation is that the molecular gas is the fuel that maintains the star formation activity (Bigiel et al. 2008; Leroy et al. 2008). If the gas supply into galaxies is continuously smooth, then the formation of stars may be driven by internal dynamical processes within the interstellar medium (ISM; Kereš et al. 2005; Bournaud et al. 2007; Dekel et al. 2009; Spring & Michałowski 2017). It is therefore essential to identify the physical processes that govern the ISM properties to tackle galaxy evolution.
A complete characterization of the ISM involves the understanding of many complex processes that are drive and evolve on different spatial and time scales. ISM models often assume a dynamic equilibrium (e.g., Thompson et al. 2005; Ostriker et al. 2010; Faucher-Giguère et al. 2013; Krumholz 2015), especially for systems with high star formation activity. The star formation activity, parametrized by the Kennicutt-Schmidt law (Kennicutt 1998a), is also evidence that additional sources of energy beyond stellar feedback may help support system self-gravity (Zhou et al. 2017). Unresolved observations for starbursts also agree with this model (Fisher et al. 2019). However, there are few that use the CO and Pa α emission lines to study the ISM dynamics in dusty starbursts.

We assume a ΛCDM cosmology with Ωm = 0.73, ΩΛ = 0.27, and H0=70 km s⁻¹ Mpc⁻¹. Thus, at a redshift range of z = 0.1 – 0.2, a spatial resolution of 0.′′6 corresponds to a physical scale between 1.0 – 1.8 kpc.

2. Observations & Data Reduction

2.1. The three targeted galaxies

We select three galaxies taken from the VALES survey at z ≈ 0.12 – 0.18. These systems were selected based on their likelihood to be molecular gas-rich systems, i.e., with expected molecular gas fractions fH₂ ≡ M/H₂/(M+M*) > 0.3 after assuming a Milky-way like CO-to-H₂ conversion factor fCO MW = 4.6 M6 (K km s⁻¹ pc⁻²)⁻¹. Our ‘gas-rich’ criterion takes into account two observational facts: (1) the negligible cosmic evolution of fH₂; (2) local galaxies have several hundred gas fractions of ~ 0.1 (Leroy et al. 2009; Saintonge et al. 2017) with only a few of these presenting fH₂ > 0.3 (% 1% based on XCO, GASS survey M*, measurements re-scaled by assuming fCO MW, Saintonge et al. 2017).

In Fig. 1 we present the global properties for these three galaxies compared to full VALES and GAMA surveys. We adopt the star-formation galaxy (SFG) ‘main-sequence’ parametrization suggested by Whitaker et al. (2012). The main-sequence corresponds to the tight correlation between the galaxy stellar masses and star formation rates (SFRs). Our three targets are representative of the starburst galaxy population.

Using the Baldwin-Phillips-Terlevich (BPT) diagram (Baldwin et al. 1981), we show that two systems lie just below the limit of the pure star-forming region (Kauffmann et al. 2003). The remaining target (HATLAS114625—014511) is located in the low ionization nuclear emission line region (LINER). The Hβ, [OII], [OIII] and [NII] flux measurements are presented in Appendix A. By using the Wide-field Infrared Survey Explorer (WISE; Wright et al. 2010) mid-IR colour diagram (right panel in Fig. 1) Stern et al. (2012) & Mateos et al. (2012), HATLAS114625—014511 would be classified as an AGN host galaxy, while the other two targets are classified as SFGs in agreement with the BPT-diagram analysis.

2.2. ALMA observations

In this work, we describe an ALMA follow-up campaign (taken from project 2015.1.01012.S: PI.: E. Ibar) for imaging three VALES galaxies for which we obtained previous bright CO(1-0) detections presented in Villanueva et al. (2017). Observations were taken on Band-3 with the extended 12 m array to obtain higher spatial and spectral resolution imaging than previous observations.

The spectral setup was designed to target the redshifted CO(1-0) emission line (between 97 GHz and 103 GHz, depend-
Fig. 1: Characterization of the three galaxies presented in this work in terms of stellar mass, SFRs, and AGN activity. Left: The SFR-$M_*$ plane. The solid and dashed lines represent the main-sequence (MS) parametrization suggested by [Whitaker et al. 2012] and the 4x SFR(MS) starburst threshold, respectively. Middle: The BPT-diagram (Baldwin et al. 1981). The dashed line shows the empirical star-forming threshold (Kauffmann et al. 2003), whereas the solid curve corresponds to the theoretical maximum starburst model (Kewley et al. 2001). These two lines encompass the SFGs-AGN ‘composite’ zone. The dotted-dashed line indicates the empirically determined AGN threshold (Schawinski et al. 2007). Right: WISE mid-IR colour-colour diagram. The solid lines delimit the AGN-zone suggested by [Mateos et al. 2012], whereas the dashed line represents the AGN threshold adopted by [Stern et al. 2012]. The WISE data 1-$\sigma$ errorbars are smaller than the plotted symbol sizes. The GAMA data are taken from their data-release 3 (GAMA-DR3; Baldry et al. 2018) encompassing galaxies at $z < 0.35$ (the upper redshift limit for the VALES survey) and with 5-$\sigma$ or higher flux estimates. These three panels indicate that the three galaxies presented in this work can be classified as starbursts, with one target (HATLASJ114625−014511) likely to be classified as an obscured AGN host galaxy.

Table 1: ALMA observational setup for project 2015.1.01012.S.

| Source List          | Observation Date | Flux Calibrator | Bandpass Calibrator | Phase Calibrator | P.W.V. (mm) | Number of antennas | Time on Target (min) | $\theta_{\text{BMAJ}}$ (arcsec) |
|----------------------|------------------|-----------------|---------------------|------------------|-------------|--------------------|----------------------|--------------------------|
| HATLASJ114625.0−014511 & HATLASJ121446.4−011155 | 9 Aug. 2016      | J1229+0203       | J1229+0203          | J1150−0023      | 0.80        | 36                 | 35                   | 0:52                     |
| HATLASJ114625.0−014511 & HATLASJ121446.4−011155 | 11 Aug. 2016     | J1229+0203       | J1229+0203          | J1150−0023      | 0.80        | 36                 | 35                   | 0:50                     |
| HATLASJ090750.0+010141 | 13 Aug. 2016     | J0854+0206       | J0854+0206          | J0909+0121      | 0.63        | 36                 | 35                   | 0:45                     |

2.3. SINFONI observations

We observe the Pa$\alpha$ emission line by using the SINFONI IFU (Eisenhauer et al. 2003) on the ESO-VLT in its seeing-limited mode (Project 099.B-0479(A); P.I. J.Molina). The SINFONI field-of-view (FOV) is 8’’×8’’ with a pixel angular size of 0.0125’. The spectral resolution is $\Delta\lambda/\Delta\lambda \sim 3800$, and OH sky-lines have $\sim 5$ Å full width at half maximum – FWHM ($\approx 30$ km s$^{-1}$ at 2.1$\mu$m). The observations were carried out in service mode between 2017 March 15 and 2017 December 11 in seeing and photometric conditions (point spread function – PSF FWHM $\approx 0^\prime\prime4$–$0^\prime\prime8$ in K-band). In addition, two different jittering patterns were used during the observing runs in order to boost the observation signal-to-noise ratio (S/N) in one galaxy.

2.3.1. ‘OSSO’ Jittering

To observe the HATLASJ1146251−014511 and HATLASJ121446.4−011155 galaxies (hereafter, HATLASJ114625 and HATLASJ121446, respectively), we used the traditional ABBA chop sequences, nodding 16′′ across the IFU. That means that the traditional jittering OBJECT-SKY-SKY-OBJECT (‘OSSO’) pattern was implemented. We used one observing block (OB) per target, implying a total...
Table 2: Spatially-integrated measurements for the three starbursts. The far-IR luminosities are calculated across the rest-frame 8–1000 µm wavelength range. $E(B – V)_{\text{Neb}}$ is the colour excess estimated by using the observed Hα-to-Paα flux ratio. SFR$_{\text{Paα}}$ and SFR$_{\text{Paα,corr}}$ correspond to the observed and attenuation-corrected Paα-based SFR estimates, respectively. $S_{\text{CO}}\Delta v$ is the velocity integrated flux density. $L_{\text{CO}}$ is the CO(1-0) line luminosity taken from Villanueva et al. (2017).

| HATLASJ090750.0+010141 | HATLASJ114625.4–014511 | HATLASJ121446.0–011155 |
|------------------------|------------------------|------------------------|
| RA (J2000)             | Dec (J2000)            | z$_{\text{spec}}$      |
| 09:07:30.07            | +01:01:41.47           | 0.1284                 |
| z$_{\text{spec}}$      |                        | 0.16553                |
| $M_*$ $(\times 10^{10} M_{\odot})$ | $L_{\text{IR}} (\times 10^{10} L_{\odot})$ | $S_{\text{CO}}\Delta v$ (Jy km s$^{-1}$) |
| 1.4±0.4                | 50±1                   | 6.8±0.6                |
| $L_{\text{IR}}$        |                        | 5.4±0.5                |
| 51±1                   | 6.6±0.6                |                        |
| $S_{\text{CO}}\Delta v$ |                        |                        |
| 6.6±0.6                |                        |                        |
| $L_{\text{CO}}$        |                        |                        |
| 8.6±0.8                |                        |                        |
| $L_{\text{CO}}$        |                        |                        |
| 7.3±0.9                |                        |                        |

observing time of $\approx$3.2 ks per source. The raw datasets for these two sources were reduced by using the standard SINFONI ESO/ESOREX data reduction pipeline.

2.3.2. ‘OOOO’ Jittering

We perform an on-source experimental jittering pattern to increase the S/N of the Paα emission line in one galaxy. In this experimental observation, the pointing was kept fixed at the galaxy location. Thus, an OBJECT-OBJECT-OBJECT-OBJECT (‘OOOO’) jitter sequence was used. Based on previous analyses by Godoy et al. (in prep), this observing approach provides reliable results for emission line with S/N$\gtrsim$15.

To reduce the data, first, we use the SINFONI ESOREX and ESO/ESOREX pipelines. Then, sky emission lines are subtracted using SkyCor (Noll et al. 2014), while MOLEFIT (Kausch et al. 2015) is implemented to remove telluric absorption bandpass lines (Godoy et al. in prep.). This is necessary as we do not have bright stars in our small sample, HATLASJ090750.0+010141 (hereafter, HATLASJ090750). By using this method, the observed emission line S/N is expected to increase by $\sqrt{N}$ compared to the use of an ‘OSSO’ jitter pattern due to the extra on-source time. For this observation, the exposure time was also set to $\approx$3.2 ks. More details about this experimental observation are reported in Appendix B.

2.3.3. Flux calibration

The standard star observation is used to perform the flux calibration. First, the galaxy spectrum is corrected in each pixel by atmospheric telluric absorptions and by the SINFONI K-band transmission curve. We do this by collapsing the standard star datacube in the spectral axis using a wavelength range free from significant telluric absorptions. A two-dimensional Gaussian function is fitted to this spectrally-collapsed image. Then, we extract the spectrum from the standard star by using an aperture size of 2×FWHM in diameter. We use this standard star spectrum to normalize the galaxy spectrum observed in each pixel. We take into account the different total exposure times.

Then, in each pixel, we multiply the normalized spectrum by a representative stellar black-body profile. To obtain this black-body curve, we fit a black-body function to the standard star magnitudes collated in the Visual Observatory SED Analyser (VOSA, Bayo et al. 2008). This allows us to estimate the stellar surface temperature – thus the black-body function shape – and the normalization constant to construct the representative standard stellar black-body profile as seen in the SINFONI K-band. We note that the typical relative uncertainty for the conversion factor is $\approx$5% (e.g., Piqueras López et al. 2012).

Even though we can provide reliable flux calibrations for HATLAS114625 and HATLAS121446, the different on-source (‘OOOO’) observing mode for HATLAS090750 impeded a proper calibration from its standard star observation. The flux calibration for this observation requires us to carefully model the sky for the standard star observation and, hence, the stellar spectrum. However, we were unable to obtain an accurate stellar atmospheric model for the standard star (HD 56006) due to its uncertain stellar parameters. More details about these uncertainties are presented in Appendix B.

2.3.4. Spatial resolution

We also use the spectrally-collapsed standard star image to determine the PSF FWHM ($\theta_{\text{PSF}}$) for each K-band observation. By fitting a two-dimensional Gaussian function, we determine $\theta_{\text{PSF}} \approx$ 0′′62, 0′′39 and 0′′81 for HATLAS090750, HATLAS114625 and HATLAS121446, respectively.

2.4. Stellar Mass and IR-based SFR estimates

The stellar masses for the three galaxies were estimated in Villanueva et al. (2017) by using the photometry provided by the GAMA survey (extending from the far-UV to FIR – $\approx$ 0.1 – 500 µm) and by using the BayesianSED fitting code MAGPHYS (Da Cunha et al. 2008). We assume a Chabrier (2003) initial mass function (IMF). The $M_*$ values are presented in Table 2.

The IR-based SFRs (SFR$_{\text{IR}}$) are estimated by using the rest-frame far-IR 8–1000 µm luminosity ($L_{\text{IR}}$) estimates taken from Ibar et al. (2015). By assuming a Chabrier (2003) IMF, the SFR$_{\text{IR}}$ values are calculated following SFR$_{\text{IR}}$ ($M_{\odot}$ yr$^{-1}$) = $10^{-10} \times L_{\text{IR}}$ ($L_{\odot}$; Kennicutt 1998) and correspond to the obscured star-formation activity. The IR-based SFRs are consistent with the
SFR estimates suggested by MAGPHYS but tend to be offset by a factor of ~ 2 toward higher values (see Villanueva et al. 2017 for more details).

2.5. CO(1-0) Luminosities

The total galaxy CO(1-0) velocity-integrated flux densities ($S_{CO(1-0)}$) are taken from Villanueva et al. (2017). Briefly, these were estimated by implementing a two-step procedure. First, the CO(1-0) line is spectrally fitted by a Gaussian profile to determine its FWHM and spectrally-collapses the datacube within ±1×FWHM. Then, $S_{CO(1-0)}$ values are estimated by fitting a two-dimensional Gaussian function to the spectrally-integrated datacube (moment 0) using the task GAUSSFIT within CASA. Finally, the CO(1-0) luminosities ($L_{CO(1-0)}$) are calculated by following Solomon & Vanden Bout (2005):

\[
L_{CO(1-0)} = 3.25 \times 10^7 S_{CO(1-0)} \Delta \nu \nu_{obs}^{-2} D_L^2 (1+z)^3 [K \text{ km s}^{-1} \text{ pc}^2],
\]

where $S_{CO(1-0)}$ is in Jy km s$^{-1}$, $\nu_{obs}$ is the observed frequency of the emission line in GHz, $D_L$ is the luminosity distance in Mpc, and $z$ is the redshift. Both estimates are presented in Table 2.

### 3. ANALYSIS and RESULTS

3.1. Average ISM properties

To analyse the spatially-integrated emission line fluxes for our three galaxies, first, we collapse the new ALMA and SINFONI datacubes into one-dimensional spectra (Fig 2). These spectra were built by stacking the spectrum seen in the individual pixels from which we detected an emission line (see § 3.2.2). Before stacking, we manually shifted the individual emission lines to rest-frame accounting for redshift and the respective pixel line-of-sight (LOS) velocity value (see Fig. 3). Thus, we try to minimize any line broadening produced by rotational motions and we focus on intrinsic individual emission line widths.

In all the starbursts, the spatially-integrated Paα emission line seems broader than the CO(1-0) emission line. By convolving the ALMA spatially-integrated spectrum by the SINFONI line spread function (LSF; green curves in Fig. 2), we find that the spectral resolution difference is not producing this trend. The difference between the spatially-integrated Paα and CO(1-0) line widths seems to be caused by broader nuclear Paα emission lines in the individual pixels in each galaxy (see § 3.2.2). The broad nuclear Paα emission lines indicate that the ionized gas ISM phase is more affected by turbulent supersonic motions than the molecular gas.2 We do not detect any broad-line component (> 500 km s$^{-1}$) in the spatially-collapsed SINFONI spectra, suggesting the absence of signatures from a broad line region produced by an active galactic nucleus (AGN).

We use the Paα emission line fluxes to derive SFR estimates (less affected by attenuation compared to H$\alpha$) using the Kennicutt (1998b)’s conversion for the Chabrier (2003) IMF. By assuming an intrinsic H$\alpha$-to-Paα ratio equal to 0.116 (Case B recombination, Osterbrock & Ferland 2006), the Paα-based

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2 For a typical H$\alpha$ region with a temperature of 104 K, we expect a Paα thermal broadening of ~ 20 km s$^{-1}$. For the molecular gas ISM phase with a temperature of £ 200 K, we expect thermally-broadened CO line widths £ 0.5 km s$^{-1}$.
SFRs (SFR$_{\text{Pas}}$) are calculated following $\text{SFR}_{\text{Pas}}(M_\odot \text{yr}^{-1}) = 4.0 \times 10^{-44} \times \text{L}_{\text{Pas}}(\text{erg s}^{-1})$. The SFR$_{\text{Pas}}$ values are presented in Table 2. We do not present an SFR$_{\text{Pas}}$ estimate for the HATLAS090750 galaxy as we were unable to obtain a reliable flux calibration for its SINFONI observation.

We compute the nebular $E(B-V)$ colour excess ($E(B-V)_{\text{Neb}}$) by using the observed Hα-to-Paα flux ratio$^3$ and assuming a Calzetti et al. (2000) attenuation law. We list the $E(B-V)_{\text{Neb}}$ values in Table 2. We note that these $E(B-V)_{\text{Neb}}$ values are ~4.7 and ~2.3 times higher than the colour excess estimates given by MAGPHYS for the stellar component ($E(B-V)_{\text{S}}$ ~0.29 and ~0.39 for HATLAS114625 and HATLAS121446, respectively). This is expected from local galaxy studies, where the higher $E(B-V)_{\text{Neb}}$ values suggest a differential attenuation model in which stars experience attenuation from a diffuse ISM dust component, but the massive young stars experience an additional attenuation as they are embedded in their dusty birth clouds (Calzetti et al. 2000). However, we note that the HATLAS114625’s nebular-to-stellar colour excess ratio is twice than the average value found in local galaxies (~ 2.3, Calzetti et al. 2000), indicating its highly dusty nature and more in line with the findings of an extreme obscured starburst galaxy population at $z \sim 0.5$–0.9 (Calabrò et al. 2018).

By considering the derived $E(B-V)_{\text{Neb}}$ values, we estimate attenuation-corrected SFR$_{\text{Pas}}$ (SFR$_{\text{Pas,corr}}$) values of $67 \pm 8$ and $40 \pm 6 \ M_\odot \text{yr}^{-1}$ for HATLAS114625 and HATLAS121446, respectively. These estimates are slightly higher than the SFR$_{\text{Pas}}$ values (Table 2), but still consistent with the 2-$\sigma$ uncertainties for both starbursts.

### 3.2. Galaxy Dynamics

We construct the two-dimensional moment maps by following Swinbank et al. (2012). Briefly, the spectrum associated with each pixel corresponds to the average spectrum calculated from the pixels inside a square area that contains the spatial resolution element – the synthesized beam or PSF. The noise per spectral channel is estimated from a region that does not contain any source emission. We use the mpfit Python package (Newville et al. 2014) to fit a Gaussian profile to the emission lines. In the case of the SINFONI observations, we mask the spectrum at the wavelength ranges where OH sky-line features are present and the Paα line widths are corrected by spectral resolution effects.

We apply an S/N = 5 threshold to determine whether we have detected an emission line or not. If this criterion is not achieved, then we increase the square binned area by one pixel per side and repeat the Gaussian fit again. We iterate up to two more times in order to avoid large binned regions. After the third iteration, if the S/N criterion has not been achieved, we mask that pixel and skip to the next one.

The pixel-by-pixel intensity, velocity and velocity dispersion 1-$\sigma$ uncertainties are estimated by re-sampling via Monte Carlo simulations the flux density uncertainties in the data. The maps from both emission lines are presented in Fig. [3].

The CO(1-0) and Paα intensity maps present smooth distributions with no clear level of clumpiness, at ~ kpc-scales, in the three starbursts. These also agree with the stellar morphology seen in K-band image. However, we note that OH sky-line features present in the SINFONI observations may add noise to the Paα two-dimensional maps and this may partly explain the smoother CO(1-0) maps as the ALMA spectra are free from sky-line residuals.

### 3.2.1. Kinematic Modelling

We model the ionized and molecular gas ISM kinematics by fitting the two-dimensional LOS velocity fields. The model velocity maps are constructed by assuming an input arctan rotation curve:

$$V(R) = V_0 + 2 \pi V_{\text{sym}} \arctan(R/R_1),$$

where $R_1$ is the radius at which the rotation curve turns over, $V_0$ is the systemic velocity (i.e. redshift) and $V_{\text{sym}}$ is the asymptotic rotational velocity (Courteau 1997).

For each observation, the kinematic model considers seven free parameters ($V_0$, $V_{\text{sym}}$, $R_1$, $P_A$, $[x/y]$, and inclination angle). We convolve the velocity model map with the PSF or synthesized beam, and we use the emcee Python package (Foreman-Mackey et al. 2013) to find the best-fit model.

We use the K-band Sérsic photometric models (Sérsic 1963) to constrain the inclination angle values. We use the K-band best-fit minor-to-major axis ratio ($b/a$; Table 3) as initial guess input to the kinematic modelling and we allow to search the best-fit inclination value within a 3-$\sigma$ range. To better account for the K-band model $b/a$ uncertainty, we adopt a $b/a$ ratio 1-$\sigma$ relative error equal to 10% as suggested by Epinat et al. (2012). The

### Table 3: K-band surface brightness Sérsic best-fit model parameters taken from the GAMA-DR3 for our sample (Kelvin et al. 2012). $\mu_{0,K}$ is the central surface brightness value. $R_{1/2,K}$ corresponds to the half-light radius. $n_S$ is the Sérsic photometric index. $P_{\alpha}$ indicates the position angle of the photometric major axis. The ellipticity $\epsilon$ is derived from the projected major-to-minor axis ratio on the sky ($\epsilon \equiv 1 - b/a$). The final column denotes the reduced chi-square ($\chi^2$) value of the best-fit model.

| Name            | $\mu_{0,K}$ (mag/arcsec$^2$) | $R_{1/2,K}$ (kpc) | $P_{\alpha}$ | $\epsilon$ | $\chi^2$ |
|-----------------|-------------------------------|-------------------|--------------|------------|----------|
| HATLAS090750    | 9.36                          | 3.66              | 4.92         | 62.1       | 0.26     | 2.19     |
| HATLAS114625    | 3.78                          | 2.76              | 6.80         | 82.2       | 0.60     | 1.29     |
| HATLAS121446    | 15.31                         | 2.55              | 1.26         | 3.5        | 0.67     | 1.12     |

In the particular case of the HATLAS090750 system, the $K$-band and Paα intensity images show two asymmetric features that may be related to gas inflow/outflow or tidal interaction. These features suggest an on-going merging process. Both features account for ~18% of the total Paα flux suggesting on-going star formation activity. One of the asymmetric features has a projected velocity blueshift of ~300 km s$^{-1}$ compared to the system centre, while the other feature presents a velocity redshift of ~80 km s$^{-1}$ suggesting that this system has a complex 3D shape. The ALMA observation just traces the CO(1-0) emission coming from the central part of this system, probably due to sensitivity limitations. Interestingly, the central part of this system shows a rotational pattern in the CO(1-0) and Paα velocity maps, with a peak-to-peak rotational velocity of $V_{\text{max}} \sin(i) \sim 90$ km s$^{-1}$.

In contrast, HATLAS114625 and HATLAS121446 show clear disc-like rotational patterns in their CO(1-0) and Paα velocity maps. The ionized and molecular gas kinematics broadly agree in both starbursts with peak-to-peak rotational velocities of $V_{\text{max}} \sin(i) \sim 360 - 460$ km s$^{-1}$, respectively.

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$^3$ The Hα flux estimates are taken from the GAMA survey DR3 (see Table A.1).
inclination angle is derived from $b/a$ by considering an oblate spheroid geometry (Holmberg 1958):

$$\cos^2(i) = \frac{(b/a)^2 - q_0^2}{1 - q_0^2},$$

where $i$ is the galaxy inclination angle and $q_0$ is the intrinsic minor-to-major axis ratio (i.e. disc thickness) of the galaxy. For edge-on systems ($i = 90$ deg), $q_0 = b/a$. We use $q_0 = 0.14$ mean
value reported for edge-on galaxies at low-redshift ($z < 0.05$). [Mosenkov et al. 2015].

The model best-fit parameters and $\chi^2_r$ values are given in Table 4 and the r.m.s. values are shown in each residual map (Fig. 3). The kinematic position angles roughly agree with each other ($\Delta PA = PA_{\text{Pa}a} - PA_{\text{CO}} \lesssim 10$ deg). For HATLAS114625 and HATLAS121446 galaxies, these also roughly agree with the position angles derived from the K-band image modelling.

The best-fit disc model gives a reasonable fit to the inner ionized and molecular gas kinematics of the HATLAS090750 galaxy as suggested by the low reported r.m.s. value. This may indicate a fast relaxation process of the ISM molecular gaseous phase into a disc-like galaxy in the central zone of this system (e.g. [Kronberger et al. 2007]. For the other two galaxies, the r.m.s. values presented in the Paα velocity residual maps tend to be larger than the values derived from the CO(1-0) observations, suggesting that the ionized gas ISM phase may be a more sensitive tracer of non-circular motions compared to the molecular gas ISM phase. However, these high r.m.s. values also are a consequence of the coarser SINFONI spectral resolution compared to the ALMA observations plus additional noise induced by the OH sky-line features present in some pixels at the wavelengths where the Paα emission line is found.

3.2.2. Kinematic Parameters

We use the best-fit dynamical models to simulate a slit observation along the major kinematic axis and we extract the one-dimensional rotation velocity and velocity dispersion curves for both ISM phases (Fig. 4). We consider a slit width equal to the synthesized beam or PSF FWHM. The half-light radii for the ionized and molecular gas ISM phases ($R_{1/2,Paα}, R_{1/2,CO}$) are calculated by using a tilted ring approach. From the rotation curve, we define the rotational velocity for the Paα and CO observations ($V_{rot,Paα}, V_{rot,CO}$) as the inclination corrected values observed at two times the Paα and CO half-light radii, respectively.

To correct the velocity dispersion values for beam-smearing effects, we apply the correction suggested by [Stott et al. 2016]. This corresponds to a linear subtraction of the local velocity gradient $\Delta v/\Delta R$ from the beam-smeread line widths. However, to further consider beam-smearing residual effects from this correction, we define the global velocity dispersion for each gas phase ($\sigma_{v,CO}, \sigma_{v,Paα}$) as the median value taken from the pixels located beyond three times the synthesized beam or PSF FWHM from the dynamical centre (white circumferences in velocity dispersion maps in Fig. 3).

For HATLAS090750, we find a very compact CO light distribution as suggested by its half-light radius. In its central zone, this system shows a low rotational velocity ($V_{rot,CO} \sim 70$ km s$^{-1}$) and a high median velocity dispersion $\sigma_{v,CO} \sim 35$ km s$^{-1}$, suggesting a molecular gas ISM phase with highly supersonic turbulent motions and a CO-traced kinematic ratio $V_{rot,CO}/\sigma_{v,CO} \sim 2$. The CO- and Paα-based rotation curves clearly agree at the radius at which CO(1-0) is detected (Fig. 4), implying that the $V_{rot,CO}$ and $V_{rot,Paα}$ values also agree.

In contrast, the Paα emission tends to show broader line widths compared to the CO emission line ($\sigma_{v,Paα} \sim 66$ km s$^{-1}$). This is unlikely to be produced by beam-smeread flux coming from the asymmetric features as the broader Paα line widths are seen across all the major kinematic axis. Assuming that the line widths trace the turbulent kinematic state of the respective ISM phase, this result suggests that the molecular gas phase may be able to dissipate the turbulent kinetic energy faster than the ionized gas phase. Another possibility could be an additional energy injection in the ionized gas from stellar feedback such as stellar winds, supernova feedback and/or Wolf-Rayet episodes (e.g. [Thornton et al. 1998, Crowther 2007, Kim & Ostriker 2015, Martizzi et al. 2015, Kim et al. 2017]). The expansion of over-pressured Hii regions is also a possibility (Elmegreen & Scalo 2004). We remind that we have corrected the SINFONI observations by instrumental line broadening effects.

For HATLAS114625 and HATLAS121446, the molecular and ionized gas ISM phases show similar scale sizes $R_{1/2,Paα}/R_{1/2,CO} \approx 0.85 \pm 0.01$ and $0.96 \pm 0.01$, respectively. For HATLAS121446, these half-light radii estimates also agree with $R_{1/2,K}$ (see Table 4). However, for HATLAS114625, we find that $R_{1/2,K}/R_{1/2,CO,Paα} \approx 1.3 - 1.6$ kpc, suggesting that the ionized and molecular gas ISM phases are distributed in a more compact disc-like structure in this galaxy.

For both starbursts, the velocity curves agree and we derive ionized to molecular gas rotation velocity ratios $V_{rot,Paα}/V_{rot,CO} \approx 1.04 \pm 0.04$ and $0.94 \pm 0.14$, for HATLAS121446 and HATLAS114625, respectively. The consistency between the CO- and Hα-based velocity curves tend to be found in local galaxies.
where the ionized gas emission seems to come from recent star formation activity episodes (Levy et al. 2018).

In both systems, the median $\sigma_{V_{\text{Pa}},\text{CO}}$ values are lower than the corresponding $\sigma_{V_{\text{Pa}},\text{Pa}}$ estimates ($\sigma_{V_{\text{Pa}},\text{Pa}}/\sigma_{V_{\text{Pa}},\text{CO}} \approx 1.5-2$), however, those still agree within 1-$\sigma$ uncertainties. The CO and Paα velocity dispersion values seen in both galaxies suggest a dominant common nature. The CO and Paα velocity dispersion profiles (Fig. 4) suggest even closer $\sigma_{V_{\text{Pa}},\text{Pa}}$ and $\sigma_{V_{\text{Pa}},\text{CO}}$ values. Nevertheless, we note that our measured $\sigma_{V_{\text{Pa}},\text{CO}}$ tend to be higher than the estimates reported from local systems ($\approx 9-19$ km s$^{-1}$, Levy et al. 2018). Indeed, these median $\sigma_{V_{\text{Pa}},\text{CO}}$ values are consistent with the lower end of the velocity dispersion estimates measured from ULIRGs ($\sim 30-140$ km s$^{-1}$, Downes & Solomon 1998, Wilson et al. 2019).

We derive an average CO-based rotational velocity to dispersion velocity ratio ($V_{\text{rot,CO}}/\sigma_{V_{\text{CO}}}$) of $\approx 3 \pm 2$ for HATLAS114625 and HATLAS121446, respectively. If we consider the Paα observations, we derive $V_{\text{rot,Paα}}/\sigma_{V_{\text{Paα}}}$ $\approx 4 \pm 2$ and $\sim 5 \pm 3$, respectively. Independent of the emission line considered, the $V_{\text{rot}}/\sigma$ ratios measured for HATLAS114625 and HATLAS121446 suggest that the rotational motions are the main support against self-gravity in both starburst galaxies.

3.2.3. Comparison with previous VALES works

Using our kpc-scale resolution data ($\sim 0''5$), we try to test if the previous kinematic analysis done for the VALES galaxies (Molina et al. 2019b) may be biased due to beam-smearing effects. These previous CO(1-0) observations were performed by using a more compact ALMA array configuration, thereby delivering a coarser spatial resolution ($\sim 3-4'' \approx 5-7$ kpc). Beam-smearing could hide galaxy morpho-kinematic properties, making it hard to recover unbiased intrinsic parameters when the spatial resolution is of the order of several kpc.

Even though the galaxies presented in this work, HATLAS114625 and HATLAS121446, were not described in Molina et al. (2019b) as they were not extended enough for a dynamical interpretation, we can still make a brief comparison with the VALES systems that share similar global properties.

We concentrate in VALES sources with similar specific SFR values ($s\text{SFR}=\text{SFR}/M_\star$; $\Delta \text{log}(s\text{SFR}) < 0.3$ dex) than the estimated for HATLAS114625 and HATLAS121446 ($s\text{SFR} = 10-100$ Gyr, respectively). For these sources, we find that the kinematic maps present marginally resolved rotation ($V_{\text{rot,CO}} \approx 40 - 200$ km s$^{-1}$) and high velocity dispersion values ($\sigma_{V_{\text{CO}}} \approx 40-70$ km s$^{-1}$), implying $V_{\text{rot,CO}}/\sigma_{V_{\text{CO}}}$ ratios in the range of 1-3. These values are lower than the ones presented in this work, suggesting that the kinematic parameters presented in Molina et al. (2019b) might be systematically biased due to beam smearing. This comparison is not straightforward as the resolution presented in this work is five to seven times higher than in Molina et al. (2019b), however, it highlights the importance of high-resolution imaging for extracting more precise dynamical information.

3.3. The CO-to-\(H_2\) conversion factor from dynamics

A CO-to-\(H_2\) conversion factor must be used to estimate molecular gas masses from the CO luminosities ($M_{\text{H}_2} = a_{\text{CO}} L_{\text{CO}}$; e.g. Bolatto et al. 2013). Traditionally, different $a_{\text{CO}}$ values have been considered to calculate $M_{\text{H}_2}$ for galaxies as a whole (Solomon & Vanden Bout 2005). An $a_{\text{CO,LMW}} \approx 4.6 M_\odot (\text{K km s}^{-1} \text{pc}^{2})^{-1}$ value seems to be more appropriate for disc-like galaxies (e.g. Solomon et al. 1987), whereas an $a_{\text{CO,ULIRG}} \approx 0.8 M_\odot (\text{K km s}^{-1} \text{pc}^{2})^{-1}$ value has been estimated for ULIRGs and assumed to be representative for merger-like systems (e.g. Downes & Solomon 1998). However, it is unlikely that $a_{\text{CO}}$ follows a bi-modal distribution. Models suggest
a smooth transition that depends on the ISM physical properties (e.g. Narayanan et al. 2012).

We exploit the dynamical mass estimate \( M_{\text{dyn}}(R) = \frac{v_{\text{circ}}^2 R}{2\sigma} \) to constrain the \( \alpha_{\text{CO}} \) value. In this procedure, we assume that the dynamical mass estimate corresponds to the sum of the stellar, molecular and dark matter masses (e.g. Motta et al. 2018; Molina et al. 2019). This is true when looking at the central regions of galaxies. The H\(_i\) component at larger scales dominates the gas mass, while the ionized gas might have a role as well. Additionally, for the sake of simplicity, we also assume a constant \( \alpha_{\text{CO}} \) value across each galactic disc. Therefore, by quantifying the dark matter content in terms of the dark matter fraction \( f_{\text{DM}} \) at each galactocentric radius, we obtain the following constraint;

\[
f_{\text{DM}}(R) = 1 - \frac{M_*(R) + \alpha_{\text{CO}} L'_{\text{CO}}}{M_{\text{dyn}}(R)},
\]

where the CO luminosities inside each radius are calculated directly from the ALMA observations and the stellar masses are truncated using the K-band Sérsic model profile following Molina et al. 2019a.

To estimate the dynamical mass values and use Eq. [4] first we need to calculate the circular velocity \( V_{\text{circ}} \) at each galactocentric radius. To do this, we consider two cases, the thin- and thick-disc hydrostatic equilibrium approximations. In the first case, the galaxy support against self-gravity is assumed to be purely rotational and \( V_{\text{circ}} \) corresponds to the observed rotational velocity \( V_{\text{circ}} = V_{\text{rot,CO}} \) Genzel et al. 2015. In the second case, the galaxy scale height cannot be neglected, and the self-gravity is balanced by the joint support between the rotational motions and the pressure gradient across the galactic disc (Burkert et al. 2010).

In this ‘thick-disc’ approximation, an analytic expression for \( V_{\text{circ}} \) can be derived by parametrizing the pressure gradients in terms of \( \sigma_v \) (which is assumed to be constant across the galactic height and radius) and the mass distribution, which we assume to follow the best-fit Sérsic model of the K-band surface brightness distribution;

\[
V^2_{\text{circ}}(R) = V_{\text{rot,CO}}^2(R) + 2\frac{\sigma^2 b_n}{n s} \left( \frac{R}{R_{1/2,k}} \right)^{(1/n_s)},
\]

where, \( V_{\text{rot,CO}} \) is the rotation velocity profile (Fig. [4], \( b_n \) is the Sérsic coefficient that sets \( R_{1/2,k} \) as the K-band half-light radius (e.g. Burkert et al. 2016; Lang et al. 2017; Molina et al. 2019b).

The disc radial coordinates are determined by the best-fit two-dimensional model. Additionally, to minimize beam-smearing effects, we only consider the \( V_{\text{rot,CO}} \) values extracted from a zone beyond three times the synthesized beam FWHM from the dynamical centre (see ‘\( \sigma_v \)’ panels in Fig. [5]). However, as we still expect some residual beam-smearing effect at these radii, we also apply a correction factor (\( \leq 10\% \)) to the rotation velocity values based on the ratio between the intrinsic-to-smoothed best-fit arctan velocity models across the galaxy major kinematic axis (Appendix D).

We note that this method suffers from a degeneracy between the \( \alpha_{\text{CO}} \) and \( f_{\text{DM}}(R) \) parameters, along with it there is a strong dependence on the accuracy of the \( M_{\text{dyn}} \) and \( M_* \) values. To try to overcome these issues, we use a Markov Chain Monte Carlo (MCMC) technique (Calistro Rivera et al. 2018; Molina et al. 2019b) implemented in emcee (Foreman-Mackey et al. 2013).

Table 5: CO-to-H\(_2\) conversion factor, molecular gas masses and gas fractions for HATLAS114625 and HATLAS121446 starbursts

|                | HATLAS114625 | HATLAS121446 |
|----------------|--------------|--------------|
| \( \alpha_{\text{CO}} \) \( M_\odot \) \((\text{K km s}^{-1} \text{ pc}^2)^{-1} \) | 0.7±0.5 | 1.2±0.6 |
| \( M_{\text{H}_2} \times 10^9 \ M_\odot \) | 6.0±4.3 | 10.3±5.7 |
| \( f_{\text{H}_2} \) | 0.11±0.07 | 0.14±0.10 |

We estimate the posterior probability density function (PDF) for the CO-to-H\(_2\) conversion factor and the dark matter fraction parameters by sampling the \( \alpha_{\text{CO}}–f_{\text{DM}}(R) \) phase-space defined in Eq. [4] and by considering the likelihood of the estimated \( L'_{\text{CO}} \), \( M_{\text{dyn}} \) and \( M_* \) values.

Additional to the thin- and thick-disc dynamical model assumptions, we explore the effect of the chosen underlying mass distribution by assuming that the galaxies follow an exponential total-mass surface density distribution (Freeman 1970). We note that this assumption produces a variation in our thick-disc \( M_{\text{dyn}} \) and truncated \( M_* \) estimates. Thus, we employ a total of four different dynamical models per galaxy.

We do not derive an \( \alpha_{\text{CO}} \) value for the HATLAS090750 system as this on-going merger may not fulfill the virial assumption necessary to obtain a dynamical mass estimate.

In Fig. [5] we show the \( \alpha_{\text{CO}} \) posterior PDFs for HATLAS114750 and HATLAS121664 starbursts. We note that the thick-disc Sérsic mass-profile model suggests slightly higher \( \alpha_{\text{CO}} \) values than the other three models for both galaxies. This is produced by two effects; (1) the additional pressure gradient support against self-gravity, which is low for our galaxies as suggested by the \( V_{\text{rot,CO}}/\sigma'_{\text{V,CO}} \approx 7 \) ratios; and (2) surface density profiles steeper than the ones derived from an exponential model profile as indicated by the Sérsic indexes \( n_g \geq 1 \). This tends to increase the \( M_{\text{dyn}} \) values by a larger amount compared to the truncated \( M_* \) values at smaller galactocentric radii.

We note that a possible systematic overestimation of \( M_* \) by MOnlinephys may bias the \( \alpha_{\text{CO}} \) estimates toward lower values than the reported ones. This scenario is unlikely as we have input a large wavelength SED coverage (~ 0.1 – 500\( \mu \)m) to obtain accurate \( M_* \) values (see also Michałowski et al. 2014). However, to be conservative, we assume \( \alpha_{\text{CO}} \) upper limit values \( \alpha_{\text{CO,uplim}} \) given by the PDFs 3-\( \sigma \) range. We obtain \( \alpha_{\text{CO,uplim}} = 2.7 \) and 5.1 \( M_\odot \) (K km s\(^{-1}\) pc\(^2\))\(^{-1}\) for HATLAS114625 and HATLAS121446, respectively.

In the remaining of this work, we estimate the molecular gas masses by adopting the median CO-to-H\(_2\) conversion factor value derived from the thick-disc Sérsic mass-profile dynamical model, i.e., by considering the model that suggests the higher median \( \alpha_{\text{CO}} \) value. This election does not affect our results as the differences between the four dynamical models are marginal compared to the uncertainties behind the galaxy estimates as seen by the broad \( \alpha_{\text{CO}} \) PDFs. Our analysis suggests low \( \alpha_{\text{CO}} \) values that are consistent with the ULIRG-like value for both starbursts. We present this value along with the molecular gas estimates in Table 5.

A direct result of adopting a \( \alpha_{\text{CO}} \) value is that our early expectation about observing ‘gas-rich’ systems was wrong. Indeed, the measured \( f_{\text{H}_2} \) values are consistent with the average estimate for local star-forming galaxies \( f_{\text{H}_2} \sim 0.1 \), Leroy et al. 2009, Saintonge et al. 2017. This suggests that these starbursts...
galaxies may not be ‘gas-rich’ as originally expected, implying that without a robust molecular gas estimate, it is not straightforward to catalogue these systems as possible analogues of the high- \( z \) SFG population.

### 4. Discussion

#### 4.1. What sets the molecular gas velocity dispersions?

HATLAS114625 and HATLAS121446 present \( \sigma_{\text{CO}} \) values that are comparable with the lower end estimates observed in ULIRGs (\( \sigma_{\text{CO}} \approx 30–140 \text{ km s}^{-1} \), Downes & Solomon 1998; Wilson et al. 2019). However, both galaxies show regular disc-like kinematics with little evidence of interactions that may enhance the internal \( \sigma_{\text{CO}} \) values, suggesting that the high molecular gas velocity dispersion values may be produced by internal secular processes.

Wilson et al. (2019) found that, in ULIRGs, the \( \sigma_{\text{CO}} \) values roughly increase with the molecular surface density (\( \Sigma_{\text{H}_2} \)), following a power-law relationship with a tentative exponent of \( \sim 0.5 \). Wilson et al. (2019) suggested that this correlation can be explained if ULIRGs are in vertical pressure balance. In this section, we explore if their model is able to explain the \( \sigma_{\text{CO}} \) values measured for the HATLAS114625 and HATLAS121446 galaxies. We choose Wilson et al. (2019)’s ISM pressure balance model because we lack of stellar velocity dispersion measurement for our sources. This quantity is required to calculate the pressure set by self-gravity in other ISM models such as, for example, in the traditional Elmegreen (1989)’s ISM model.

In Wilson et al. (2019)’s model, a downward pressure on the molecular gas (modelled as a gas layer) is produced by the disc self-gravity, plus an additional contribution from the dark matter halo. This pressure can be calculated as;

\[
P_{\text{grav,W+19}} = 0.5 \pi G \Sigma_{\text{H}_2} \Sigma_{\text{Tot}} (1 + \gamma),
\]

where \( \Sigma_{\text{Tot}} \) is the disc total mass surface density and \( \gamma \) is a factor that accounts for the vertical pull toward the galaxy midplane produced by dark matter. This factor depends inversely on \( V_{\text{rot}}/\sigma_{\text{rot}} \) squared, thus, it contributes a small correction for both galaxies (\( \gamma \approx 0.05 \)).

The upward pressure is parametrized as a function of the average mid-plane density \( \rho_{\text{mid}} \) and the thermal plus turbulent velocity dispersions;

\[
P_{\text{ISM}} = \rho_{\text{mid}} \sigma_{\text{H}_2}^2 (1 + \psi) = \frac{\Sigma_{\text{H}_2} \sigma_{\text{H}_2}^2 (1 + \psi)}{2 h_{\text{H}_2}},
\]

where \( \rho_{\text{mid}} = \Sigma_{\text{H}_2} / 2 h_{\text{H}_2} \), \( h_{\text{H}_2} \) is the molecular gas disc scale height, \( \sigma_{\text{H}_2} \) is the molecular gas velocity dispersion (hereafter we assume \( \sigma_{\text{H}_2} \approx \sigma_{\text{CO}} \)) and \( \psi \) is a factor which accounts principally for the magnetic-to-thermal support ratio (\( \sim 0.3 \), Kim & Ostriker 2015) as the cosmic ray to turbulent support ratio is negligible (see Wilson et al. 2019 for more details).

The vertical equilibrium condition requires \( P_{\text{grav,W+19}} = P_{\text{ISM}} \) and allows us to write the Wilson et al. (2019)’s Eq. 6 in a more compact form:

\[
h_{\text{H}_2} = \frac{\sigma_{\text{H}_2}^2}{\pi G \Sigma_{\text{Tot}} (1 + \gamma)}.
\]
SFG data correspond to ~kpc-scale measurements for a main-sequence galaxy presented in Molina et al. (2019a).

Despite of comparing with data observed at different spatial resolutions, both starbursts exhibit \( \sigma_{\text{rot}} \) values mainly in the range between the local SFGs and ULIRGs, but their ~kpc-scale \( \Sigma_v \) values are comparable to the average estimates measured for the local SFGs and much lower than the estimates reported for the ULIRG sample. However, similar to the ULIRGs, the starburst data seem to follow a roughly \( \sigma_{\text{rot}} \propto \Sigma_{\text{H}_2}^{0.5} \) power-law relationship. This is shown by the dashed line which represents the pressure balance model suggested by Wilson et al. (2019), but scaled to the average \( \Sigma_{\text{H}_2} / \Sigma_{\text{rot}} \) and \( \sigma_{\text{rot}} / \Sigma_{\text{H}_2} \) ratios measured for both systems. Additionally, the solid line shows Wilson et al. (2019)’s model for the local ULIRGs.

We now consider the total surface density \( \Sigma_{\text{rot}} \) (Fig. 6). We approximate \( \Sigma_{\text{rot}} \) by the sum of \( \Sigma_{\text{H}_2} \) and the stellar surface density \( \Sigma_\star \) (\( \Sigma_{\text{rot}} \equiv \Sigma_{\text{H}_2} + \Sigma_\star \)). For each starburst, the pixel-by-pixel \( \Sigma_\star \) values are calculated by scaling the SINFONI K-band continuum image surface brightness distribution (Fig. 5) to the global \( M_\star \) value derived by magphys.

HATLAS114625 and HATLAS121446 starbursts tend to be located in the lower \( \Sigma_{\text{rot}} \) limit covered by the ULIRG sample. Despite of the large scatter (\( \approx 0.22 \) dex, for non-masked values), the vertical pressure balance model (solid line) gives a reasonable representation of the data. We note that the systematic uncertainty added by the adopted \( \alpha_{\text{CO}} \) conversion factor is low as the \( \Sigma_{\text{rot}} \) values are mainly dictated by \( \Sigma_\star \) in both starbursts (sources have low integrated molecular gas fractions; see Table 5). The change is probably increased by the use of a constant mass-to-light ratio to estimate \( \Sigma_\star \).

By using Eq. 8 we estimate roughly \( h_{\text{H}_2} \) for both starbursts. We plot the \( h_{\text{H}_2} \) pixel-by-pixel distribution in the right panel of Fig. 6. From the non-masked pixels, we obtain \( h_{\text{H}_2} \approx 200_{-130}^{+160} \) and \( 160_{-80}^{+30} \) pc median values for HATLAS114625 and HATLAS121446, respectively. Those values are consistent with the average estimate reported for the ULIRG systems (~ 150 pc; Wilson et al. 2019).

Our data support the scenario in which the molecular gas velocity dispersion on large scales (~kpc-scales) is set by the local gravitational potential of the galaxy through the reaching of the vertical pressure balance as suggested by Wilson et al. (2019).

We note that, the main difference between the two starbursts analysed in this work and the ULIRGs presented by Wilson et al. (2019) is that, in the former, the vertical gravitational pressure is mainly dictated by the stellar component (\( f_\text{H}_2 \approx 0.1 \)) and not by a nearly equal gravitational contribution from stars and gas. Indeed, if in Eq. 6 we take the approximation \( \Sigma_{\text{rot}} \approx \Sigma_\star \) and we assume vertical pressure equilibrium, then we obtain \( \sigma_{\text{rot}} \propto \Sigma_\star^{1.5} \), suggesting that, even in starburst systems, the molecular gas dynamical properties can be set by the stellar gravity.

Momentum injected by stellar feedback may be insufficient to produce the observed \( \sigma_{\text{rot}} \propto \Sigma_{\text{rot}} \) trend. Hydrodynamical simulations suggest that stellar feedback can just account for \( \sigma_{\text{rot}} \) values up to ~6–10 km s\(^{-1}\) for the diffuse gas component and with a moderate increase with gas surface density (Ostriker & Shetty 2011; Shetty & Ostriker 2012). However, our data sample the \( \sigma_{\text{rot}} \gtrsim 15 \) km s\(^{-1}\) range and additional pressure sources, such as stellar feedback, may still set the \( \sigma_{\text{rot}} \) values below this limit.

Resolution effects should be present as our ~kpc-scale measurements may underestimate the ambient pressure at smaller scales. This effect has been recently measured by high-resolution (~60 pc) molecular gas observations in nearby galaxies (Sun et al. 2020). Indeed, Sun et al. (2020) suggest a correction for the ~kpc-scale pressure estimates. However, their observations cover a considerably lower galactic pressure range (~\( 10^{4.5} \) K cm\(^{-2}\)), see Fig. 8 and, thus, extrapolating such a correction and applying it to our measurements is uncertain. Nevertheless, these high-resolution observations also suggest that the
molecular gas is in pressure balance with its weight and the local ISM self-gravity (see also Schruba et al. 2019).

Another major caveat in our analysis comes from the assumption behind Eq. 6. This equation corresponds to a corrected form of the Spitzer (1942) formula for an isothermal layer embedded in a spherical mass component. It does not consider a multi-component composition of the ISM and may not be appropriate to describe the vertical pressure produced by a gaseous plus stellar ISM. For example, in the traditional Elmegreen (1989)’s ISM pressure formula, the $\Sigma_s$ term is weighted by the ratio between the molecular-to-stellar velocity dispersions ($s \equiv \sigma_{v,CO}/\sigma_{*,s}$). In this case, the additional vertical pressure set by $\Sigma_s$ can be neglected in the limit $s \ll 1$. Only if $s \sim 1$, then Eq. 6 is recovered. Thus, Eq. 6 should be considered as an upper limit case of the Elmegreen (1989)’s formula.

4.2. The star-formation activity traced at ~kpc-scales

Our CO(1-0) and Paα observations are ideal for studying the star formation activity in dusty starburst galaxies. The CO(1-0) emission provides a direct estimate to the molecular gas mass (albeit an $\alpha_{CO}$), and Paα does not suffer from significant extinction (compared to Hα), facilitating a direct view to the star formation activity in dustier environments.

The star formation activity can be described as a power-law relationship between the SFR surface density ($\Sigma_{SFR}$) and total gas surface density ($\Sigma_{gas}$) or $\Sigma_{H_2}$, the well-known Kennicutt-Schmidt relationship (Kennicutt 1998a). For typical local star-forming galaxies, when $\Sigma_{H_2}$ is used, it is well-characterized by a linear relation with an observed average molecular gas depletion time $\tau_{dep}$ = $\Sigma_{H_2}/\Sigma_{SFR}$ = 2.2 ± 0.3 Gyr (Leroy et al. 2013). However, this linear trend seems not to be followed by galaxies with enhanced SFRs as those tend to exhibit shorter molecular gas depletion times or higher star formation efficiencies (SFE$\equiv \tau_{dep}^{-1}$, e.g. Daddi et al. 2010).

In Fig 7 we show the pixel-by-pixel distribution in $\Sigma_{SFR}$ versus $\Sigma_{H_2}$ plane for HATLAS114625 and HATLAS121446. The $\Sigma_{SFR}$ and $\Sigma_{H_2}$ quantities are directly estimated from the spatially-resolved SINFONI and ALMA observations assuming the median $\alpha_{CO}$ value (Table 5) and employing the dynamical modeling to correct by projection effects.

We use the HST/STScI task written in the Interactive Data Language (IDL) to register the images on the same pixel scales and orientation. While implementing this routine, we consider that the total flux is conserved in each map. We prefer not to include the HATLAS090750 system in our analysis due to its complex geometry and uncertain $\alpha_{CO}$ value.

We compare our $\Sigma_{SFR}$–$\Sigma_{H_2}$ estimates with ~kpc-scale local galaxy measurements and the ~sub-kpc data from local ULIRGs. Briefly, the ~kpc-scale data are represented by the median trend reported from the HERA CO-Line Extragalactic Survey (HERACLES, Leroy et al. 2008) for normal star-forming systems and measurements from two LIRGs (NGC3110 and NGC232; Espada et al. 2018). The local ULIRG data correspond to CO(1-0)-based ~350-650 pc-scale estimates presented in Wilson et al. (2019).
The two galaxies presented in this work exhibit $r_{\text{dep}}$ values in the range of $\sim 0.1$–1 Gyr, i.e., $r_{\text{dep}}$ values comparable to that derived for ULIRGs ($r_{\text{dep}} \leq 0.1$ Gyr), but in a low $\Sigma_{\text{HI}}$ environment. $r_{\text{dep}}$ internal galactic trends are not clear due to the considerable data scatter.

If we assume our $\alpha_{\text{CO,uplim}}$ estimates, we obtain $r_{\text{dep}}$ median values of $\sim 0.5$ and 0.6 Gyr for HATLAS114625 and HATLAS121446, respectively. In this case, both starbursts mainly present $r_{\text{dep}}$ values within 0.2 – 2.2 Gyr, a range similar to that reported for the two local LIRGs (0.2–1.6 Gyr; Espada et al. 2018). In any case, the depletion times estimated for both galaxies are lower than the $r_{\text{dep}}$ median values reported for local SFGs with similar $\Sigma_{\text{HI}}$, and $f_{\text{HI}}$ values (Leroy et al. 2013). It suggests that the enhancement of the SFE seen in starburst galaxies may not be only related to high $\Sigma_{\text{HI}}$ estimates.

### 4.3. Pressure regulated star-formation activity

If the star-formation activity also depends on the dynamics of the molecular gas, then $\Sigma_{\text{SFR}}$ should also correlate with the physical variables that regulate these properties. Thus, if the vertical pressure equilibrium sets the molecular gas properties on larger scales (e.g., kpc-scales, § 4.1), then $\Sigma_{\text{SFR}}$ should correlate with the ISM pressure set by self-gravity $P_{\text{grav}}$. The correlation between $\Sigma_{\text{SFR}}$ and ISM pressure has been suggested and observed previously by many authors (e.g., Genzel et al. 2010; Ostriker et al. 2010; Ostriker & Shetty 2011; Bolatto et al. 2017; Herrera-Camus et al. 2017; Fisher et al. 2019) and also used to explain the so-called “extended” Kennicutt-Schmidt relation (Shi et al. 2011). Indeed, the mid-plane hydrostatic pressure seems to predict the star formation efficiency better than gas surface density in atomic-dominated regimes (Leroy et al. 2008).

In Fig. 8, we show $\Sigma_{\text{SFR}}$ as a function of $P_{\text{grav}}$. The Physics at High Angular resolution in Nearby Galaxies (PHANGS; Leroy et al. in prep.) data correspond to measurements from 28 nearby galaxies presented in Sun et al. (2020) and artificially convolved to kpc-scale by them. We also consider the spatially-resolved ULIRG data presented in Wilson et al. (2019) and The HI Nearby Galaxy Survey (THINGS; Walter et al. 2008; de Blok et al. 2008) and DYNAMO (Green et al. 2014) galactic averages presented in Fisher et al. (2019). We caution, however, that the DYNAMO pressure data are based on galactic ionized gas velocity dispersion measurements along with spatially-unresolved molecular gas observations (Fisher et al. 2019). We also present the $\sim$kpc-scale values measured for a typical star-forming galaxy at $z \sim 1.5$ (SHI-ZELS-19; Molina et al. 2019a). The dashed line corresponds to the best-fit presented by Fisher et al. (2019) for the DYNAMO and THINGS data, while the solid black line corresponds to the best-fit given by Sun et al. (2020) to the PHANGS data. The dot-dashed line corresponds to the parametrization given by Kim et al. (2013) for their set of hydrodynamical simulations. The solid red line represents our best-fit. The starburst and ULIRG data are consistent with the trend reported from the nearby galaxies. The $z \sim 1.5$ star-forming galaxy data are in clear offset.

Our best-fit estimates agree within 1-$\sigma$ uncertainty with the values reported for the DYNAMO (Fisher et al. 2019) and THINGS data ($N = 0.76 \pm 0.06$, log$_{10}(P_{\text{pk}}/[\text{cm}^{-3}\text{K}]) = 5.89 \pm 0.35$). However, we find that Fisher et al. (2019)’s best-fit is offset from the kpc-scale data by $\sim 0.5$ dex, suggesting that their result was probably affected by the assumptions behind using unresolved CO data.

Sun et al. (2020) report $N = 0.84 \pm 0.01$ and log$_{10}(P_{\text{pk}}/[\text{cm}^{-3}\text{K}]) = 5.85 \pm 0.01$ best-fit estimates for the PHANGS data, but they caution that their best-fit uncertainties may be underestimated due to not considering systematic errors. This problem may be affecting our uncertainty estimates as well.

To compare with their result, we estimate the r.m.s. of the best-fit residuals. We measure r.m.s. $\approx 0.34$ and $\approx 0.36$ dex from our and Sun et al. (2020) best-fits, respectively. We note that these values are considerably increased by considering the $z \sim 1.5$ SFG data. However, these data seem to be an outlier compared to the other kpc-scale measurements and, perhaps, it is produced by an underestimated dust extinction correction applied to the observed SFR for this system. If we do not consider
the $z \sim 1.5$ SFG data, we find r.m.s. $\approx 0.25$ dex from both best-fit residuals. Thus, in both cases, we obtain a good agreement between our and Sun et al. (2020) results.

The stellar feedback regulated model predicts a $\Sigma_{\text{SFR}}$ and ISM pressure balance with the slope close to unity (Ostriker & Shetty 2011). In this model, stellar feedback (e.g. photoionization, radiation, supernovae, winds) heats the ISM gas while the energy and pressure losses occur via turbulent dissipation and cooling. The star formation activity gives pressure support against self-gravity (hence, $P_{\text{IM}} = P_{\text{grav}}$). $\Sigma_{\text{SFR}}$ and $P_{\text{ISM}}$ are closely related due to a nearly constant injected feedback momentum per stellar mass formed $\Sigma_{\text{SFR}} = 4(p_{\text{ff}}/m_*) P_{\text{ISM}}$; e.g. Ostriker et al. (2010) [Ostriker & Shetty 2011]; Shetty & Ostriker 2011.

This is highlighted by the dot-dashed line in Fig. 8 which represents the best-fit power-law ($N \approx 1.1$) for the hydrodynamical simulations presented in Kim et al. (2013). This power-law overestimates the ISM pressure for the ULIRG systems. However, those systems display larger $\Sigma_{\text{SFR}}$ values than that covered by the simulations ($\Sigma_{\text{SFR}} \lesssim 10^{-2} M_{\odot}$ yr$^{-1}$ kpc$^{-2}$; Kim et al. 2013). To further test the plausibility of $\Sigma_{\text{SFR}} \propto P_{\text{grav}}$ trend, we fit a linear function to our data. We obtain a best-fit intercep value $\log_{10} (P_{\text{ff}}/kpc^{2}c^{3}/M_{\odot}) = 6.74 \pm 0.01$ (we caution that the uncertainty may be underestimated due to systematic errors) and a residual r.m.s. of $0.047$ and $0.031$ dex depending on whether we include the $z \sim 1.5$ SFG data or not. The r.m.s. values are slightly higher than the reported estimates from our previous best-fit. The intercep value translates to $p_{\text{ff}}/m_* \sim 4600$ km s$^{-1}$, a value that is $1.5$ times higher than the estimate typically adopted for single supernovae feedback ($\sim 3000$ km s$^{-1}$; e.g. Thornton et al. 1998; Martizzi et al. 2015; Ostriker & Shetty 2011; Kim & Ostriker 2015). Enhanced feedback from clustered supernovae may be needed to explain such a $p_{\text{ff}}/m_*$ value (e.g. Sharma et al. 2014; Gentry et al. 2017). However, for the effectiveness is still under debate. (Gentry et al. 2019).

Additional energy sources that regulate the star formation activity should also be considered. Mass transport through the galactic disc could be one of these (e.g. Krumholz et al. 2018). Nevertheless, this may require understanding how the gas dissipates the gravitational energy from larger scales toward smaller scales (e.g. Bournaud et al. 2010; Combes et al. 2012) until the range where the stellar feedback operates and stops the local gravitational collapse through momentum/energy injection. In this picture, the observed star formation activity occurs as a response to the ISM pressure balance.

It is also worth mentioning that Sun et al. (2020) calculated $P_{\text{grav}}$ by using the ‘dynamical equilibrium pressure’ ($P_{\text{DE}}$ e.g. Elmegreen 1989; Wong & Blitz 2002; Ostriker et al. 2010; Ostriker & Shetty 2011; Fisher et al. 2019) which accounts for the gas and stellar galaxy self-gravity in the limit in which the gas disc scale height ($h_{\text{gas}}$) is much smaller than the stellar disc scale height ($h_{*}$; Benincasa et al. 2016). They neglect the gravitational pressure set by the dark matter component as this pressure source is small in galaxies analysed by them. It is also the case of our galaxies and the ULIRGs presented in Wilson et al. (2019). We determine $P_{\text{grav}}$ by using Eq. 6. This equation corresponds to a $P_{\text{DE}}$ upper limit case when $h_{\text{gas}} \approx h_{*}$ (see Appendix A of Benincasa et al. 2016). Thus, a possible correction to our $P_{\text{grav}}$ estimates may lead to a steppe $\Sigma_{\text{SFR}} \propto P_{\text{grav}}$ correlation.

Another possible source of uncertainty comes from the limited spatial resolution from our observations. Beam-smearing effect produces that $\Sigma_{\text{SFR}}$ and $\Sigma_{\text{H}i}$ (hence, $P_{\text{grav}}$) are average ~ kpc-scale estimates of the patchy underlying surface density distributions. This artificial dilution effect is quantified for the PHANGS molecular gas data (see Sun et al. 2020 for more details), however, it is unknown for the starburst galaxy population where the ISM is denser. Higher spatial resolution observations ($\sim 10 \sim 100$ pc) may further be needed to quantify this.

4.4. Limitations of our dynamical mass approach

One of the stronger constraints for the dynamical modelling is given by the assumption of a constant CO-to-$H_2$ conversion factor across the galactic disc. This may not be an ideal assumption due to possible $\alpha_{\text{CO}}$ variation with galactocentric radius (e.g. Sandstrom et al. 2013). Indeed, lower $\alpha_{\text{CO}}$ values are likely to be measured towards the Galactic centre (Bolatto et al. 2013). Based on the dynamical mass modelling, it is highly uncertain to determine an $\alpha_{\text{CO}}$ radial variation due to the unconstrained dark matter fraction values. We need to assume a halo model. However, we cannot accurately constrain the halo properties as the observed rotation curves do not extend more than ~6 kpc away from the galactic centre (Fig 4). A constant $\alpha_{\text{CO}}$ assumption is reasonable given our data limitations.

The dynamical interpretation is mainly limited by the degeneracy between $\alpha_{\text{CO}}$ and $f_{\text{DM}}$ values constrained at the inner galactocentric radius considered in each galaxy ($R \approx 2.3$ kpc, Fig 4). The over/under-estimation of $f_{\text{DM}}$ at this radius will bias our result towards lower/higher $\alpha_{\text{CO}}$ estimates. In the case that we are underestimating $f_{\text{DM}}$, then the median $\alpha_{\text{CO}}$ values should be considered as an upper limit of the true values, implying that both starburst galaxies might have lower molecular gas masses and $\alpha_{\text{CO}}$ values even lower than that reported for ULIRGs.

On the other hand, a possible overestimation of the $f_{\text{DM}}$ does not affect our results. If we assume the limit case that there is no dark matter, then the median $\alpha_{\text{CO}}$ values increase by $\leq 14\%$ compared to these estimated values when the dark matter content is considered. This variation is smaller than the $\alpha_{\text{CO}}$ PDF’s $1-\sigma$ range and it is independent of the dynamical mass model assumed (see Fig. 5).

Another limitation comes from the adopted dynamical mass formula. We have not considered any geometrical factor that should multiply the $V_{\text{rot}}/\text{CO}$ values in Eq. 5. This is equivalent to the assumption of spherical geometry when calculating enclosed mass estimates from rotational motions. However, this source of uncertainty is expected to not affect our conclusions. For example, the $V_{\text{rot}}$ difference between an exponential disk and the equivalent spherical mass distribution is $\lesssim 15\%$ and it highly depends on the disc radius (see Fig. 2.17 in Binney & Tremaine 2008). By adopting this $V_{\text{rot}}$, difference value (translated into the enclosed mass difference), then the median $\alpha_{\text{CO}}$ values would increase by $\sim 30\%$. Again, this variation is smaller than the estimated $\alpha_{\text{CO}}$ PDF’s $1-\sigma$ range.

The CO(1-0) emission source is also a concern. From our ~kpc-scale observations, we can not separate between the CO(1-0) emission originated in GMCs and any significant molecular gas diffuse emission. This diffuse component may not be negligible in galaxies (e.g. Goldsmith et al. 2008; Schinnerer et al. 2010) and it is enhanced in dense and high ISM pressure galactic environments (Sandstrom et al. 2013). If the diffuse molecular gas phase dominates the CO(1-0) emission, then low $\alpha_{\text{CO}}$
Fig. 9: Median CO-to-\textsubscript{H\textsubscript{2}} conversion factor estimates as a function of the total surface density. The grey circles correspond to the $\alpha_{\text{CO}}$ values based on dust emission for nearby disc galaxies (Sandstrom et al. 2013). The ULIRG data correspond to the estimates presented in Downes & Solomon (1998) and Papadopoulos et al. (2012). In the latter case, we show the $\alpha_{\text{CO}}$ values reported from their ‘one-’ and ‘two-component’ multi-transition models. The color bands indicate the traditional CO-to-\textsubscript{H\textsubscript{2}} conversion factors and their uncertainties for Milky Way- and ULIRG-like systems (Bolatto et al. 2013). The green line corresponds to the $\alpha_{\text{CO}}$ parametrization suggested by Bolatto et al. (2013) for galaxies with solar metallicity. For HATLAS114625, we find a lower $\alpha_{\text{CO}}$ estimate than the expected value from Bolatto et al. (2013)’s parametrization. In the case of HATLAS121446, we find an agreement within 1-$\sigma$ uncertainty. Figure adapted from Bolatto et al. (2013).

values may underestimate the high density molecular gas mass content for both starbursts (Papadopoulos et al. 2012). This effect is highlighted by the difference in the estimated $\alpha_{\text{CO}}$ values between the ‘one-’ and ‘two-component’ models for ULIRGs (Fig. 9) see Papadopoulos et al. (2012).

However, it should be noted that molecular gas diffuse emission and its contribution to the estimated $\alpha_{\text{CO}}$ values are uncertain. The CO-to-\textsubscript{H\textsubscript{2}} conversion factor may vary significantly for this gas component depending on local environment properties (e.g. Liszt & Pety 2012). Additional observations tracing the dense molecular gas phase may help to determine whether our $\alpha_{\text{CO}}$ estimations are biased toward low values or not.

We note that we have not considered the H\textsubscript{i} content in our dynamical mass approach as we expect a negligible amount of H\textsubscript{i} mass within the inner radius ($R \approx 2.3$ kpc) at which $M_{\text{dyn}}$ was calculated. We remind that the $M_{\text{dyn}}$ values calculated at these radii are the ones that strongly constrain the $\alpha_{\text{CO}}$ estimates in our procedure. In local spirals, the transition between an H\textsubscript{2} to H\textsubscript{i}-dominated ISM ($\Sigma_{\text{H\textsubscript{2}}} \approx \Sigma_{\text{H\textsubscript{i}}}$) occurs at $\Sigma_{\text{gas}} \sim 12 \pm 6$ $M_{\odot}$ pc\textsuperscript{-2} (Leroy et al. 2008). From the spatially-resolved CO(1-0) observations and the adopted $\alpha_{\text{CO}}$ values, we estimate $\Sigma_{\text{H\textsubscript{2}}} \sim 146 \pm 93$ and $127 \pm 50$ $M_{\odot}$ pc\textsuperscript{-2} at $R \approx 2.3$ kpc for HATLAS114625 and HATLAS121446 galaxies, supporting our assumption.

Finally, we check if our $\alpha_{\text{CO}}$ estimates are reasonable given by the theoretical expectation (Bolatto et al. 2013). From theories, it is expected that $\alpha_{\text{CO}}$ mainly varies with the system metallicity and total surface density. However, before making any comparison, we note that HATLAS114625 and HATLAS121446 present supra-solar metallicity values in terms of the gas phase oxygen abundance ($12 + \log(O/H) = 8.99$ and 8.72, respectively). We note that above the solar metallicity, we do not expect any significant variation of $\alpha_{\text{CO}}$ due to the high metal content (Bolatto et al. 2013). Thus, we simply assume a solar metallicity when comparing with Bolatto et al. (2013)’s theoretical prediction. We show this comparison in Fig. 9. We find that the reported median CO-to-\textsubscript{H\textsubscript{2}} values are somewhat lower than the theoretical expectation, but still consistent within the scatter. Our $\alpha_{\text{CO}}$ estimates are, therefore, reasonable given the measured $12 + \log(O/H)$ and $\Sigma_{\text{Tot}}$ values for both starbursts.

5. Conclusions

We present new ALMA Cycle-3 and VLTI-SINFONI observations tracing the CO(1-0) and Pa\textalpha emission lines from three starburst galaxies at $z \sim 0.12$–0.18 taken from the VALES survey. The ALMA observations were designed to deliver spatially-resolved observations of the molecular gas content at $\sim 0.5$, i.e., approximately the seeing-limited SINFONI observations ($\sim 0''4 - 0''8$). Combining near-IR and sub-mm observations, we study the ionized and molecular gas dynamics at ~kpc-scales.

One target, HATLAS090750, presents highly asymmetric morpho-kinematics, suggesting an on-going merger. From its SINFONI observation, we also detected fainter ro-vibrational warm molecular gas transitions along with an ionized Helium line in its central galactic zone. The H\textbeta emission lines were used to determine a warm molecular gas temperature of $\sim 1700 \pm 500$ K (Fig. 3), probably produced by supernovae remnant shocks. However, we could not discard non-thermal gas excitation sources due to the lack of H\textbeta emission line intensity measurements with different vibrational energy levels (e.g. Davies et al. 2003).

The other two starburst galaxies, HATLAS114625 and HATLAS121446, show disc-like morpho-kinematics, with rotation as the dominant component supporting self-gravity ($V_{\text{rot}}/\sigma_{\text{v}} \sim 7 - 8$). For both systems, we model the CO and Pa\textalpha galactic dynamics and we aid the kinematic modelling by using K-band photometric models to constrain the inclination angle parameter. From those analyses, we find that the CO and Pa\alpha dynamics present a good agreement in both galaxies (Fig. 3), as suggested by similar kinematic position angles ($\Delta$PA $\sim 4$ deg.) and emission line spatial extensions ($R_{1/2,\text{Pa\alpha}}/R_{1/2,\text{CO}} \sim 1$). Our observations suggest that the ionized and molecular gas components display roughly the same galaxy morpho-kinematics.

We estimate the total mass budget for both, HATLAS114625 and HATLAS121446 galaxies, by calculating the dynamical masses assuming the ‘thin-’ and ‘thick-disc’ hydrostatic equilibrium approximations (Burkert et al. 2010) along with two different surface density profile models. We obtain $\alpha_{\text{CO}}$ values in the range of $0.7$–$1.2$ ($K$ km s\textsuperscript{-1} pc\textsuperscript{2}) for both galaxies (Fig. 5), i.e., similar values to that reported for ULIRGs (Downes & Solomon 1998). These values do not depend strongly on the hydrostatic equilibrium and total surface density assumptions. Our conversion factor estimates are somewhat lower but still consistent with the $\alpha_{\text{CO}} \propto \Sigma_{\text{Tot}}^{-0.5}$ trend suggested from theoretical expectations (Fig. 5) Bolatto et al. (2013).

By adopting the dynamically based $\alpha_{\text{CO}}$ values, we obtain molecular gas fractions of the order of $\sim 0.1$ for both starbursts,

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\footnote{We base our metallicity estimates on the Pettini & Pagel (2004) calibration scale and the [N\ii] and H\alpha line intensities reported in Table A1. We also adopt a solar abundance of $12 + \log(O/H) = 8.69$ (Asplund et al. 2009).}
far below our initial expectations and consistent with values measured in local star-forming galaxies. Therefore, the sources are not ‘gas-rich’ as initially thought, highlighting the difficulties to estimate molecular gas masses due to the uncertainty of the CO-to-H$_2$ conversion factor.

We find that the HATLAS114625 and HATLAS121446 molecular gas velocity dispersion values are reasonably represented by a $\sigma_{\text{tot}} \propto \Sigma^2_{\text{H}_2}$ trend, where $\Sigma_{\text{tot}}$ is the total galaxy surface density (Fig. 6). This suggests that the molecular gas velocity dispersion values are consistent with being set by the galaxy self-gravity to maintain the vertical pressure balance.

We study the star formation activity traced at $\text{kpc}$-scales in HATLAS114625 and HATLAS121446 starbursts. Both galaxies exhibit $\tau_{\text{dep}}$ values in the range of $-0.1$--$1$ Gyr (Fig. 7), i.e., values consistent with the reported estimates for ULIRGs ($\tau_{\text{dep}} \sim 0.1$ Gyr). However, both systems present $\Sigma_{\text{H}_2}$ values that are comparable to those seen in local star-forming disc galaxies (Leroy et al. 2013). This suggests that the decrease of $\tau_{\text{dep}}$ (or enhancement of SFE) is also produced by additional physical processes that may not only be related to high $\Sigma_{\text{H}_2}$ environments.

To further explore this, we study the correlation between $\Sigma_{\text{SFR}}$ and the gravitational pressure $P_{\text{grav}}$ in HATLAS114625 and HATLAS121446 fill the gap between the normal galaxies and the ULIRG systems in terms of pressure set by $\Sigma_{\text{H}_2}$. We find a linear relation in the log-log space, $\log_{10}(\Sigma_{\text{SFR}}) = N \times \log_{10}(P_{\text{grav}}/P_0) + 0.78 \pm 0.01$, where $N = 5.38 \pm 0.04$ (Fig. 8). It is in agreement with the trend reported for local galaxies (Sun et al. 2020), suggesting that, in these $-0.12$--$0.17$ dusty starburst galaxies, the star formation activity can be a consequence of the ISM pressure balance.

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Larkin, J. E., Armus, L., Knop, R. A., Soifer, B. T., & Matthews, K. 1998, ApJS, 114, 59
Lefever, K., Pals, J., Morel, T., et al. 2010, A&A, 515, A74
Leroy, A. K., Walter, F., Bigiel, F., et al. 2009, AJ, 137, 4670
Leroy, A. K., Walter, F., Brinks, E., et al. 2008, AJ, 136, 2782
Leroy, A. K., Walter, F., Sandstrom, K., et al. 2013, AJ, 146, 19
Levy, R. C., Bolatto, A. D., Teuben, P., et al. 2018, ApJ, 860, 92
Lisz, H. S. & Pety, J. 2012, A&A, 541, A58
Madau, P. & Dickinson, M. 2014, ARA&A, 52, 415
Madau, P., Ferguson, H. C., Dickinson, M. E., et al. 1996, MNRAS, 283, 1388
Martizzi, D., Faucher-Giguère, C.-A., & Quataert, E. 2015, MNRAS, 450, 504
Mateos, S., Alonso-Herrero, A., Carrera, F. J., et al. 2012, MNRAS, 426, 3271
Michałowski, M. J., Hayward, C. C., Dunlop, J. S., et al. 2014, A&A, 571, A75
Molina, J., Ibar, E., Smail, I., et al. 2019a, MNRAS, 487, 4856
Molina, J., Ibar, E., Villanueva, V., et al. 2019b, MNRAS, 482, 1499
Mosenkov, A. V., Sotnikova, N. Y., Reshetnikov, V. P., Bizyaev, D. V., & Kautsch, S. J. 2015, MNRAS, 451, 2376
Motta, V., Ibar, E., Verdiago, T., et al. 2018, ApJ, 863, L16
Narayanan, D., Krumholz, M. R., Ostriker, E. C., & Hernquist, L. 2012, MNRAS, 421, 3127
Newville, M., Stensitzki, T., Allen, D. B., & Ingargiola, A. 2014, LMFIT: Non-Linear Least-Square Minimization and Curve-Fitting for Python
Niemczura, E., Morel, T., & Aerts, C. 2009, A&A, 506, 213
Oliva, E., Moorwood, A. F. M., & Danziger, I. J. 1990, A&A, 240, 453
Osterbrock, D. E. & Ferland, G. J. 2006, Astrophysics of gaseous nebulae and active galactic nuclei
Ostriker, E. C. & Shetty, R. 2011, ApJ, 731, 41
Ostriker, J. P., Choi, E., Ciotti, L., Novak, G. S., & Proga, D. 2010, ApJ, 722, 642
Papadopoulos, P. P. & Scquiaquist, E. R. 1999, ApJ, 516, 114
Papadopoulos, P. P., van der Werf, P., Xilouris, E., Isak, K. G., & Gao, Y. 2012, ApJ, 751, 10
Pettini, M. & Pagel, B. E. J. 2004, MNRAS, 348, L59
Piqueras López, J., Colina, L., Arribas, S., Alonso-Herrero, A., & Bedregal, A. G. 2012, A&A, 546, A64
Rífler, R., Rodríguez-Ardila, A., Aleman, I., et al. 2013, MNRAS, 430, 2002
Saintonge, A., Catinella, B., Tacconi, L. J., et al. 2017, ApJS, 233, 22
Sánchez, S. F., Kennicutt, R. C., Gil de Paz, A., et al. 2012, A&A, 538, A8
Sandstrom, K. M., Leroy, A. K., Walter, F., et al. 2013, ApJ, 777, 5
Schawinski, K., Thomas, D., Sarzi, M., et al. 2007, MNRAS, 382, 1415
Schinnerer, E., Weiß, A., Aalto, S., & Scoville, N. Z. 2010, ApJ, 719, 1588
Schulze, A., Kriejksen, J. M. D., & Leroy, A. K. 2019, ApJ, 883, 2
Seiré, J. L. 1963, Boletin de la Asociacion Argentina de Astronomia La Plata Argentina, 6, 41
Sharma, P., Roy, A., Nath, B. B., & Shchekinov, Y. 2014, MNRAS, 443, 3463
Shetty, R. & Ostriker, E. C. 2012, ApJ, 754, 2
Shi, Y., Helou, G., Yan, L., et al. 2011, ApJ, 733, 87
Solomon, P. M., Rivolo, A. R., Barrett, J., & Yahil, A. 1987, ApJ, 319, 730
Solomon, P. M. & Vanden Bout, P. A. 2005, Annual Review of Astronomy and Astrophysics, 43, 677
Spitzer, Lyman, J. 1942, ApJ, 95, 329
Spring, E. F. & Michałowski, M. J. 2017, MNRAS, 471, L101
Stern, D., Assef, R. J., Benford, D. J., et al. 2012, ApJ, 753, 30
Sternberg, A. 1989, ApJ, 347, 863
Stott, J. P., Swinbank, A. M., Johnson, H. L., et al. 2016, MNRAS, 457, 1888
Sun, J., Leroy, A. K., Ostriker, E. C., et al. 2020, arXiv e-prints, arXiv:2002.08964
Swinbank, A. M., Sobral, D., Smail, I., et al. 2012, MNRAS, 426, 935
Tacconi, L. J., Genzel, R., Neri, R., et al. 2010, Nature, 463, 781
Tacconi, L. J., Genzel, R., Saintonge, A., et al. 2018, ApJ, 853, 179
Thompson, T. A., Quataert, E., & Murray, N. 2005, ApJ, 630, 167
Thornton, K., Gaudlitz, M., Janka, H. T., & Steinmetz, M. 1998, ApJ, 500, 95
U, V., Medling, A. M., Inam, H., et al. 2019, ApJ, 871, 166
Varadhan, M. R., Croom, S. M., Lewis, G. F., et al. 2020, MNRAS, 495, 2265
Villanueva, V., Ibar, E., Hughes, T. M., et al. 2018, MNRAS, 470, 1888
Walter, F., Brinks, E., Dib, K., et al. 2008, AJ, 136, 2785
Whitaker, K. E., van Dokkum, P. G., Brammer, G., & Franx, M. 2012, ApJ, 754, L29
Wilson, C. D., Elmegreen, B. G., Bemis, A., & Brunetti, N. 2019, ApJ, 882, 5
Wolniewicz, L., Simbotin, I., & Dalgarno, A. 1998, ApJS, 115, 293
Wong, T. & Blitz, L. 2002, ApJ, 569, 157
Wright, E. L., Eisenhardt, P. R. M., Mainzer, A. K., et al. 2010, AJ, 140, 1868
Zhou, L., Federrath, C., Yuan, T., et al. 2017, MNRAS, 470, 4573
Appendix A: Emission line and WISE colour fluxes

Table A.1: Summary of the emission line and WISE colour fluxes used in this work and taken from the GAMA DR3 (Baldry et al., 2018). W1, W2, and W3 correspond to the ‘profile-fit photometry’ WISE filter fluxes measured at 3.4, 4.6 and 12 µm (Cluver et al., 2014). The uncertainties indicate 1-σ errors. Our three galaxies are catalogued as unresolved by WISE.

| Model                  | HATLAS090750 | HATLAS114625 | HATLAS121446 |
|------------------------|--------------|--------------|--------------|
| f_0          (× 10^{-17} erg/s/cm^2) | 552±16       | 76±23        | 29±11        |
| f_{OIII}     (× 10^{-17} erg/s/cm^2) | 402±14       | 196±34       | 11±8         |
| f_Ha        (× 10^{-17} erg/s/cm^2) | 2680±33      | 307±18       | 588±25       |
| f_[NII]     (× 10^{-17} erg/s/cm^2) | 1016±17      | 444±17       | 28±17        |
| W1 (mJy)    | 1.15±0.03   | 1.57±0.03    | 0.59±0.02    |
| W2 (mJy)    | 1.04±0.03   | 2.40±0.05    | 0.66±0.02    |
| W3 (mJy)    | 16.89±0.41  | 11.99±0.34   | 8.65±0.35    |

Appendix B: Experimental observation results

We performed an on-source experimental jittering pattern to optimise the S/N of the Paα emission line for HATLAS090750. In this experimental observation, the pointing was kept fixed at the galaxy location. Hence, an ‘OOOO’ jitter sequence was used. As we do not observe the sky during this observation, then the emission and telluric absorption bandpass lines need to be subtracted using sky models. We specifically used the SkyCox and MolCox pipelines. It implies that the performance of this experimental observation is mainly limited by the accuracy of the sky emissio

Appendix C: Near-IR emission lines

Near-IR emission lines are useful to determine the excitation mechanism of the gaseous material that is responsible for the emission. In this work, we measured the near-IR emission lines from the SINFONI K-band wavelength range for the later two galaxies. The upper emission line flux limits are calculated as r.m.s.×σ_{Paα,ch}, where the r.m.s. values are estimated within a 30 channel spectral window width centred at the expected emission line location in the spectra, and σ_{Paα,ch} is the Paα emission line width.

Table C.1: Spatially-integrated Brγ,1.944µm, ro-vibrational H2(1-0)S(3)/1.957µm, H2(1-0)S(2)/1.033µm, H2(1-0)S(1)/1.225µm and HeI/2.058µm fluxes relative to the Paα emission line flux. We note that the H2(1-0)S(1) emission is redshifted out of the SINFONI K-band wavelength range for the later two galaxies.

| Model                  | HATLAS090750 | HATLAS114625 | HATLAS121446 |
|------------------------|--------------|--------------|--------------|
| Brγ/Paα               | 0.05±0.002   | <0.12        | <0.08        |
| H2(1-0)S(3)/Paα       | 0.063±0.005  | 0.107±0.006  | 0.08         |
| H2(1-0)S(2)/Paα       | 0.028±0.006  | <0.17        | <0.33        |
| H2(1-0)S(1)/Paα       | 0.072±0.016  | —            | —            |
| HeI/Paα               | 0.051±0.006  | <0.27        | <0.29        |

From the central brightest pixels from our SINFONI K-band observations, we detected more near-IR emission lines than only Paα (Fig. 2). By considering a circular aperture with a radius equal to the PSF FWHM and centred at the galaxy Paα luminosity peak, we measure several other emission lines fluxes (see Table C1). These values are estimated by fitting a Gaussian function to each emission line in the spatially-collapsed spectrum and the 1-σ uncertainties are derived by bootstrapping via Monte-Carlo simulations the flux-density errors. These ratio values are corrected by assuming a Calzetti et al. (2000) attenuation law (A_{Paα} = 0.145 A_V, A_{Brγ} = 0.132 A_V, A_{HeI} = 0.113 A_V, A_{H2(1-0)S(3)} = 0.130 A_V, A_{H2(1-0)S(2)} = 0.117 A_V, A_{H2(1-0)S(1)} = 0.103 A_V). We note that this correction is determined by the shape of the assumed attenuation law.

We can only apply the near-IR emission line analysis to the HATLAS090750 galaxy as we lack enough H2 emission line flux measurements for the other two systems. For this galaxy, we use the Paα flux intensity to differentiate between the possible excitation mechanisms. The other option, the use of the Brγ emission line, is impeded given that this emission line is redshifted out of the SINFONI K-band wavelength range. This means that the H2(1-0)S(1)/Brγ ≈ 0.8 ratio that differentiates between star-forming regions and SNR shocks and compact AGN activity is translated to H2(1-0)S(1)/Paα ≈ 0.07 (assumption of Brγ-to-Paα intrinsic ratio of 12.19 (Case B recombination, Osterbrock & Ferland 2006)).
properties from this emission line as we lack of the detection of additional Hei emission lines (e.g. Benjamin et al. 1999).

We further characterize the HATLAS090750’s ISM warm molecular gas phase by using the log \( N_{\nu,j}/g_{\nu,j} \) − E excitation diagram (Davies et al. 2003). In this diagram, \( N_{\nu,j} \) is the molecular column density, \( g_{\nu,j} \) is the statistical weight and \( E \) is the upper energy level of the ro-vibrational transition. From the H\(_2\) emission line fluxes \( f_{\nu,j} \), the column densities in the upper ro-vibrational levels are computed as:

\[
N_{\nu,j} = \left( \frac{4\pi f_{\nu,j}}{A_\nu \Omega} \right) \left( \frac{\lambda}{hc} \right),
\]

where \( \Omega \) is the spectrum extraction aperture size, \( A_\nu \) is the Einstein coefficient computed by Wolnieicz et al. (1998) and \( \lambda/hc \) is the photon energy. Additionally, the \( N_{\nu,j}/g_{\nu,j} \) ratios need to be normalized to a specific population distribution \( N_{\nu0,j}/g_{\nu0,j} \) given from a determined H\(_2\) transition. We normalize them to the inferred value from the H\(_2\)\((1-0)S(3)\) emission line transition (e.g. Bedregal et al. 2009). We note that, if the warm molecular gas phase is in LTE, then the data are well described by a simple linear function that represents a Boltzmann distribution characterized by a single excitation temperature.

In Fig. C.1 we show the excitation diagram. As we lack of H\(_2\) emission line intensity measurements with different vibrational energy levels, we can only measure rotational temperature \( T_{rot} \) for the vibrational H\(_2\)(\( \nu = 1 - 0 \)) transition. We find that the data are well-fitted by a linear fit with \( T_{rot} \approx 1600\pm400 \) K, suggesting that the warm H\(_2\) ISM phase in the central brightest zone of this galaxy is in LTE.

This temperature value also suggests that the warm H\(_2\) gas may be mainly heated by SNR shocks (Brand et al. 1989; Oliva et al. 1990), with perhaps some contribution from thermal X-ray heating from SNRs (\( T_{rot} \gtrsim 2000 \) K, e.g. Draine & Woods 1990). Thermal UV heating is unlikely as models suggest lower temperature values (\( T_{rot} \lesssim 1000 \) K, Sternberg 1989). However, we stress that we can not rule out non-thermal UV excitation (e.g. fluorescence; Black & van Dishoeck 1987) as well as lack of H\(_2\) emission line observations with different vibrational energy levels (Bedregal et al. 2009).

Nevertheless, our \( T_{rot} \) estimate is slightly higher but still consistent with the average value (\( < T_{rot} > \sim 1360\pm390 \) K) reported for local (\( z < 0.08 \)) LIRGs (U et al. 2019).

Appendix D: Beam smearing effect on the rotation velocity values

Accurate rotation velocities can not be derived toward the centre of galaxies due to beam-smearing effects. Rotation velocities tend to be underestimated due to the flux-weighted nature of the data convolution with the PSF and/or synthesized beam. Thus, a beam-smearing correction needs to be applied.

Based on our best-fit two-dimensional models, we quantify the beam-smearing effect on rotation velocities by computing the beam-smereed to intrinsic \( \alpha_C \) best-fit velocity model ratio and measured across the galaxy major kinematic axis. We show the estimation of this ratio in Fig. D.1 for the ALMA and VLT-SINFONI observations of HATLAS114625 and HATLAS121446 galaxies. We find that a moderate beam-smearing correction (\( \lesssim 10\% \)) needs to be applied to the rotation velocity values measured at a galactocentric radius longer than 1.5x projected synthesized beam/PSF FWHM. At smaller radii, the beam-smearing effect tends to increase dramatically.

Appendix E: SINFONI K-band continuum maps

In Fig. E.1 we show the continuum maps used to calculate the pixel-by-pixel \( \Sigma_u \) values. These maps are scaled to the respective galaxy \( M_u \) value, i.e., by assuming a constant mass-to-light ratio across the galactic disc.

Appendix F: Full \( \alpha_{CO} \) and Dark Matter PDFs

Our dynamical mass approach is limited by the degeneracy between \( \alpha_{CO} \) and the dark matter fraction \( \rho_{DM} \) variables. Due to our assumption of a constant \( \alpha_{CO} \) value across the galactic disc, then
the dynamical mass value estimated at the innermost galactocentric radius limits the maximum $\alpha_{\text{CO}}$ value that can be obtained. At this radius, $f_{\text{DM}}$ is consistent with zero, but it does not necessarily hold at longer radii.

In Fig. E.1 we show the $\alpha_{\text{CO}}$ and $f_{\text{DM}}(R)$ PDFs derived from the ‘thick-disc plus Sérsic’ dynamical mass model, i.e. the model that determines the adopted median $\alpha_{\text{CO}}$ value in our work. There is no major difference between the $\alpha_{\text{CO}}$ PDF obtained from this model and those derived from other dynamical models as the broad $\alpha_{\text{CO}}$ PDF shapes probe (Fig. 5).

HATLAS114625 galaxy shows a higher increase of $f_{\text{DM}}$ as a function of galactocentric radius compared to the HATLAS121446, suggesting that baryonic matter is distributed more compactly in this system. It is consistent with the reported $K$-band Sérsic index value (Table 3) and the steeper velocity gradient that is seen in HATLAS114625 (Fig. 4).
Fig. F.1: Corner plot for $\alpha_{\text{CO}}$ and $f_{\text{DM}}(R)$ variables for HATLAS114625 (Top) and HATLAS121446 (Bottom) starbursts.