A Global Regulation Inducing the Shape of Growing Folded Leaves

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Abstract
Shape is one of the important characteristics for the structures observed in living organisms. Whereas biologists have proposed models where the shape is controlled on a molecular level [1], physicists, following Turing [2] and d’Arcy Thomson [3], have developed theories where patterns arise spontaneously [4]. Here, we propose that volume constraints restrict the possible shapes of leaves. Focusing on palmate leaves (with lobes), the central observation is that developing leaves first grow folded inside a bud, limited by the previous and subsequent leaves. We show that the lobe perimeters end at the border of this small volume. This induces a direct relationship between the way it was folded and the final unfolded shape of the leaf. These dependencies can be approximated as simple geometrical relationships that we confirm on both folded embryonic and unfolded mature leaves. We find that independent of their position in the phylogenetic tree, these relationships work for folded species, but do not work for non-folded species. This global regulation for the leaf growth could come from a mechanical steric constraint. Such steric regulation should be more general and considered as a new simple means of global regulation.

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Introduction
Leaves fascinate for their shape diversity. They can be simple, with lobes (palmate), with leaflets (compound), or dissected with holes. On one single plant, the leaf shape varies, sometimes strongly (heterophilly). Until now, botanists have proposed two mechanisms to explain leaf forms. The first mechanism is based on localised enhancements and reductions of growth of the free margin of the embryonic leaf [5–6], which create the peaks and the valleys of the leaf border [7–8]. The second mechanism is the death of patches of cells (programmed cell death, PCD) that forms perforations in the leaf during the lamina development. When perforations are positioned near the leaf contour, the marginal tissue eventually breaks, as in Philodendron Monstrosa (Araceae, monocotyledon), resulting in a deeply dissected blade (pinnatisect) [9]. A particular case has been described for the dissected shape of palm leaves (Arecaceae, monocotyledons). The leaf first develops with many folds, along which PCD eventually takes place, creating cuts [10].

These two mechanisms are general so that they can be tuned to reproduce the final shape of any leaf. They conceptually apply for a flat leaf during its expansion and do not take into account the

Figure 1. Developing embryonic leaves of Acer pseudoplatanus. For such opposite decussate phillotaxy, a pair of symmetric leaves develop simultaneously. The primordia first expand over the stem apex (A) and then the two symmetric leaves meet (B), limiting each other in their future growth (C–E): a first lateral fold has appeared between the central and the lateral veins (C), a second one (D), and a secondary vein on the central one (E). Pictures A, B and D are MEB pictures courtesy of Isabel Le Disquet from IFR 83 of UPMC-Paris 6. Pictures C and E are optical microscope pictures. doi:10.1371/journal.pone.0007968.g001
actual geometry of the growing leaf inside the bud. Only the last case takes into account this geometry, through the folds. Folds have been recently highlighted for their mechanical importance in thin sheets [11–12] and are ascribed to play a role in the expansion of hornbeam leaves [13]. Focusing on palmate leaves, we found that most of them are first growing folded inside a bud. We show here that these folds have a direct influence on the final shape of the leaf.

Leaves are highly organised botanical elements. They originate from small groups of cells (primordia) protruding around the shoot apex (fig. 1A). From the beginning they present a fundamental
asymmetry: the side turned toward the stem axis (adaxial) will become the smooth and shiny upper side of the leaf turned toward the light; the other side, turned toward outside (abaxial), present hairs and veins protruding and will become the lower side of the leaf.

Once the leaf has grown, it can be noticed that the final vein pattern is organised and hierarchical. Along a central vein runs majors lateral veins, radiating from the petiole, at the base of the leaf. The secondary veins branches out from them, and so on and so forth. It is also noticeable that in palmate leaves the vein hierarchy is related to the leaf shape (see figure 2). Each lobe corresponds to a major vein ending at its tip. Lobes and veins have the same hierarchy; the central vein (CV) corresponds to the largest lobe, with lateral lobes corresponding to other main lateral

Figure 5. Local relationship between synclinal folds and sinuses on immature leaves before their expansion outside the bud. Synclinal fold angles $\phi$ are measured from side views on folded leaves extracted from buds (A and C). Leaves are then unfolded to measure the corresponding sinus opening angle $\psi$ from a top view (turning the back in b, and turning the top in d). The fold, setting the sinus whose contours locally superimpose, is the symmetry axis of the sinus. If the leaf is a folded flat surface, this symmetry simply makes $\psi = 360^\circ - 2 \phi$, as sketch in B and D. This relation (line) is checked for many folds on different leaves and species. The fact that it works shows that even if the leaves grow folded in the bud (figure 3), they are already flat. The plot also shows the large range of angle variation within one species and for all the species. Pictures are two extreme cases: when the fold angle become close to 90° the valley disappears (Malva, left), while when it becomes close to 180°, the valley becomes a simple cut (Tetrapanax, right). The studied palmate leaf species belong to different order of eudicots. Following the APG II classification *Acer pseudoplatanus* and *Acer campestre* (Sapindales), *Malva sylvestris* and *Alchemilla vulgaris* (Malvales) are Rosids, *Tetrapanax papyriferum* (Apiales) is an Asterid and *Gunnera manicata* is a Gunnerale.

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The XIXth century.

This fact has been noticed early, but overlooked since up to a rare third order lobes (TV).

veins (LV), secondary lobes corresponding to secondary veins (SV), up to a rare third order lobes (TV).

In buds, leaves grow in a limited space defined by previous and following leaves. To keep on expanding its future lamina within this confined space, leaves either enroll (convolute, revolute or involute), or fold (plicate and palmate leaves) [14–15]. This fact has been noticed early, but overlooked since the XIXth century.

Results

Our first remark is that in palmate leaves, folds are not irregular but strictly follow the leaf organisation and hierarchy (see figure 3). Following the leaf asymmetry, the folds showing the abaxial (lower) epidermis outside (anticlinal folds) are very different than the opposite ones, showing the adaxial (upper) epidermis outside (synclinal folds). The anticlinal folds coincide with the main veins and follow their hierarchy (figure 3A). This relation is inclusive: an anticlinal fold always corresponds to a main vein while many veins do not correspond to any fold. On the contrary, synclinal folds do not correspond to any major vein and are rather crossed only by the smallest ones (figure 3B). Thus we call them “anti-veins”.

Our second and main observation is that the whole perimeter of folded leaves growing inside a bud is located at a particular place. For Palmate leaves it is located on the adaxial side, at the border of the folding volume, toward the central axis of the stem (see figure 4). As the leaf margin links the end of synclines to the end of anticlines, this last property induces strong relationships between the shape of the leaf and the way it was folded inside the bud. This is similar to Kirigami (‘cut-paper’ in Japanese), where a piece of paper can take any shape by folding it in a particular way, and then cutting it on one side [16].

The first consequence is that with these particular folds, and with the leaf perimeter turned adaxially, anticlines set peaks (or lobes) and synclines set valleys (or sinuses) of the unfolded leaf. As anticlines correspond to main veins, this results in the lobes surrounding the main veins. Even more, for the folded leaf, the two sides of the perimeter superimpose around a fold. The peak and sinus must then be symmetric around the fold. This seems natural for lobes, but Figure 5 shows this local property for sinuses on immature leaves extracted from buds of various species.

This Kirigami property not only induces local geometric relationships in immature leaves, but also global ones that are kept in the mature leaves, determining their final shape. Using the relation between the folds and the main veins (first and second order), mature leaves can be folded back like we expect they were when growing in the bud. Figure 6 shows various mature leaves folded this way. One can see that the whole leaf perimeter collapses onto a simple curve, even for asymmetric leaves. The different leaf shapes can then be ascribed essentially to the variation of angles between the veins and to the different curves delimiting the folded leaf. Within a single species, the change in the number of lobes can just be ascribed to a change in the number of folds (see figure 7).

This property can be translated into quantitative relationships between the length of veins and anti-veins and the angles between them. Sharing the same perimeter once folded induce that the lobes and sinuses follow some proportionality. These relationships, restraining the range of possible shapes, are shown in the case of sycamore leaves in figure 8. As well as in figures 3 and 6, these relationships hold for palmate species widely separated on the evolutionary scale (APG II classification) [17], while more closely related species with leaves that do not grow folded inside the bud show no trace of such organization. This is shown in figures 9 and 10, for Philodendron bipenifolium (Araceae) leaves. Even though it presents lobes, it grows enrolled inside its protective envelope (figures 9A, 9B). When the leaf contour is folded following the veins and anti-veins (fig. 8c), the contour does not coincide (figure 9D). When the geometrical prediction is checked, the points are scattered on the whole plane (figure 10).

The previous geometrical relationship can be intuitively translated, allowing to recognize at first sight a Kirigami leaf

Figure 6. Mature leaves of different species, numerically folded back. The leaf contour is pink. Primary and secondary veins are respectively blue and green. Primary and secondary anti-veins are yellow and red respectively. Only veins ending at peaks are represented and stand for anticlinal folds along segments linking two consecutive branching points or a branching point to a peak. Synclinal folds run along segments (anti-veins) linking a sinus to the branching point of the two surrounding veins. The thickness of the leaf is not taken into account and the leaf is folded back onto a plane, holding the angles to two surrounding veins. The thickness of the leaf is not taken into account and the leaf is folded back onto a plane, holding the angles to two surrounding veins.
Kirigami in Leaves

Acer pseudoplatanus leaves: pictures and numerical folding (same representation as figure 6). A: One lobe leaf, with only one anticlinal fold. B: Three lobe leaf, with two lateral anticlinal and three synclinal folds. C: Five lobe leaf, with four lateral anticlinal and five synclinal folds, and several secondary folds (as in figure 6A). The secondary folding is necessary here to obtain a refolding of the contour on a simple curve (see figure 13). One lobe leaves are found on new sprouts.
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Discussion

These observed geometrical relationships relate directly to the way leaves grow folded. These folds develop successively around the main veins. At the same time, a leaf lobe grows around each main vein. From a genetic point of view, each lobe can be seen as a new independent primordium. The same KNOX gene is expressed both at the place of appearance of a primordium and at the appearance of a new lobe [18]. As well the same CUC gene is expressed both at the separation between the primordium and the meristem, and in between the new lobes [19]. But what correlates the development of these lobes so that the final result fits this Kirigami property, bringing the lobe perimeters at the same volume border? The answer could be contact regulation, as mechanical contacts are known to regulate the global expansion and growth of plants [20–21].

Based on many observations of dissected buds at different stages (figure 1), we can write the following scenario for the development of the leaf inside the bud. The leaf primordium first develops, with a central vein and a flat lamina (figure 1A). It extends over the meristem apex, until it reaches the other leaves (figure 1B). The fact that it stops and will never overpass this limit indicates a first contact regulation of the growth. Later on, secondary veins being already there [22], folds appear. We think that these main veins have an active role in the formation of the folds: they rotate the lamina around them, creating the synclinal folds. This active folding pushes the rest of the developing lamina toward the inside, inducing rounded anticlinal folds (figure 1C). The lobes develop around these folded main veins, but the developing lamina stops its growth when reaching the volume border, indicating the again a contact regulation of the growth (figure 1D).

Thus the development of the lobes depends on the folding around the main veins. This active process can be triggered by the lateral mechanical constraint, but not necessarily, as neo-formed leaves can develop outside the bud and still fold themselves. Further phenomena, like PCD in the case of palm leaves, or inhomogeneous growth in the case of oaks, can also intervene to eventually shape the final leaf form once it is outside the constraining volume of the bud.

Even though growing folded in the bud, it is remarkable that the embryonic leaf can be unfolded nearly as flat as the final leaf (figure 5). This already proves a strong and permanent regulation to keep the leaf lamina flat locally [1]. But to have an overall flat surface, the folds, where this regulation mechanism cannot apply, have also to be considered. If the folds are straight, as elongating veins tend to be, then the overall surface can be flat. A problem remains around the synclinal folds, that are not restricted a priori to be straight. Indeed some leaves exhibit curved synclinal folds, and then a characteristic half-saddle unflatenable shape at their sinus.

The evolutionary interest of such folding mechanisms could be not to regulate the final shape of the leaf, but to protect the very fragile immature leaves. A good way to protect them is to grow them inside buds with protecting scales. In the limited volume of
the bud, one way to develop the largest surface, ready to catch light, is to grow folded. We found that the leaves grow with their own internal dynamics, create folds, and stop when reaching the constraining surface. This overall growth regulation is a simple way to ensure that the whole volume is evenly occupied, and that no space is lost (see figure 12). Indeed, buds are always completely full with no free space remaining. The asymmetric development of the folds (figure 1), with the fragile lamina pushed toward the more protected adaxial side, and the more robust veins, often with hairs, covering the whole abaxial side, could also be evolutionary interesting. Not only the bud scales, but also this asymmetrical folding geometry, protect the leaf from cold, dryness, and the numerous small predators (insects). The leaf shape, with its lobes, could just be a secondary consequence of the interplay of the optimization and protective mechanisms, achieved through the folding and the growth contact regulation. This explains the observation of the predominance of palmate leaves in cold-temperate regions [23], where this protection is most needed. The variations in duration and volume development before outside expansion could finally explain the continuous variation of shapes and the number of lobes.

This global mechanical regulation of the shape could happen in leaves as their shapes are, like phyllotaxis [4], just the consequence of a packing problem and not essential for their reproduction success, contrary to the shape of flowers, that have to be more directly controlled [24]. The evolutionary pressure on leaves is to grow protected, as large and as soon as possible, whatever the growth conditions. It can be more efficiently achieved with the folding and global regulation that we proposed. The presence of this Kirigami property along the whole evolutionary tree also shows that is not a highly fixed and stabilized property.
Conclusion

We are the first to reveal that the shape of palmate leaves, even though varying a lot on one branch of a tree, with lobes of different sizes, grow folded and follow this simple Kirigami property of a perimeter folding back on a simple curve. We observed this property on many species widely spread on the phylogenetic tree. Throughout our observations, on all the available species (including those from botanical gardens), we found only a few exceptions like Philodendron bipenifolium. This property of growing folded with a protected perimeter also extends to other types of leaves such as pinnate and pluri-pinnate leaves.

The kirigami property leads to geometric consequences, that we checked on young and mature leaves. This property originates from the folding of growing leaves and we insist on its importance for the final leaf shape. This folding stage and its regulation is necessary to bridge the gap between the very first primordia stages of development, which is being thoroughly studied, and the final shape of the leaves. The fact that the perimeter of these different folded lobes fall at the same border reveal a regulation process, aimed at filling perfectly the bud volume, and we propose it to be a mechanical contact regulation.

The regulation processes revealed by this leaf development study (the folding of the leaf around the veins, the mechanically sensitive leaf margin, and the overall flatness of the leaf), deserve to be more studied, and in particular their underlying molecular mechanisms. Our shape theory also points out how much the simple physical constraint of growing inside a finite volume can have an important effect, widely underestimated up to now. The theory could have implications on final shapes of organs whenever the growth is limited inside a constraining volume, such as lungs, liver or crabs legs. It finally shows how little is still known of the various shapes and their origin, not to speak of their control.

Materials and Methods

Materials

Acer pseudoplatanus, Acer campestre, Malva sylvestris, Alchemilla Vulgans, Ribes nigrum and Matus plantanifolium leaves were picked either in October either in June in different gardens and forest in and around Paris, France. Philodendron bipenifolium leaves originate from the green houses of the botanical garden of the Serre d’Auteuil, Paris, France. Sida hermaphrodita Leaves come from the Botanical Garden of the Jardin des plantes (National Museum of Natural History). Tetrapanax papyrifer leaves come from our lab specimens, Pheonix Botanical garden in Nice, and Val Rahmeh Botanical garden in Menton. Pelargonium cuculatum Leaves come from the Botanical garden of Bern (Bern University), Switzerland.

Buds of Acer pseudoplatanus and other species were collected in late spring. Neo-formed leaves get their shape (folds) when they are bigger than pre-formed leaves which pass fall and winter in buds.
It makes both the dissection and the observation of the first development stages easier.

**Scanning Electron Microscopy**

The tissues were fixed within a 2% of glutaraldehyde in 0.1 M phosphate buffer solution of pH 7.4, for 7 hours. After having been rinsed with PBS they were immersed for 1 hour in a phosphate buffer solution with 1% of osmium tetroxide. They were then rinsed in water. The specimens were dehydrated through a graded alcohol series. They were dried in a critical point dryer (CPD7501 polaron) with liquid carbon dioxide. Dried specimens were coated with a gold layer about 40 nm thick with a sputtering (scancoat six sputter coater Boc Edwards). Preparations were observed with a S 260 Cambridge SEM, operating at 10 kV.

**Analyses**

For the sinus opening angles, as in figure 5, the immature leaves are dissected from the buds. A photography is made of each fold, side view, and then unfold, top view. The angles are measured from the pictures.

For the numerical folding (as in figures 6, 7 and 9) and measurements (as in figures 8, 10 and 11), the unfolded mature leaf is pictured on a red background, allowing to extract numerically (by color contrast) the perimeter of the leaf (figure 13A). Then on the picture the main veins and secondary veins are drawn (by hand), keeping the numerical coordinates (see File S1). If only the main veins are used, we draw them straight from the petiole to the tip (figure 13B). Deviations from the real veins are usually small. High deviation indicates an important

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**Figure 10. Geometric relationships between two successive lobes and sinuses coming from the Kirigami property, for the enrolled Philodendron bipenifolium leaf.** Same notations and plots as in figure 8. A: Two consecutive primary lobes have veins of lengths $R_a$ and $R_b$. They are respectively making an angle $\alpha$ and $\beta$ with the anti-vein, of length $R_c$, between them. B: The vein of length $R_c$ is surrounded by two anti-veins of lengths $R_a$ and $R_b$. These are respectively making angle $\alpha$ and $\beta$ with the vein. As in figure 8, the predictions of the Kirigami property are compared to the measured values for veins (C) and for anti-veins (D). Points represent 85 Philodendron bipenifolium leaves. For each leaf, all pair of consecutive primary veins or anti-veins (four for the presented leaf) have been measured. One observes that points are scattered in both figures. This figure, together with the previous one, shows that the Kirigami property does not appear for any shape.

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Figure 11. Simplified relationship on two successive lobes and sinuses that can be used to recognize the Kirigami property. As in figure 8, the graphs express the relation between the folds length and the angles. A: Length ratio (Ra/Rc) of two consecutive main veins in function of the difference (α–β) between the angles there are making with the anti-vein. The smaller the angle, the smaller the vein. If the anti-vein (sinus) is at the middle between the two veins, then the two veins have the same length (ratio 1, right inset). On the contrary, if the angle for the second lobe becomes small, then the length of the second lobe should be smaller, eventually becoming equal to the length of the anti-vein or sinus (left inset). B: Length ratio (Rb/Rd) of two consecutive main anti-veins in function of the difference (β–γ) between the angles with the vein. Similarly, the relation express that the smaller the angle, the longer the anti-vein. When the angles are equal the two anti-veins have the same length (right inset), while if one angle becomes smaller, the corresponding anti-vein becomes longer, eventually becoming equal to the vein (left inset). Contrary to figure 8, these relations are approximate, scattering the points. They are exact only if the opening angle of the lobes is constant, which is a first approximation, but in practice mixes different relationships for each lobe opening angle. However, they are simple way to judge of the Kirigami property, judging by the eye the ratio of length and angle difference, that the anti-veins and veins are axes of symmetry of the contour. For instance they are clearly wrong for figure 10B (is smaller than 1, but Ra is much longer than Rc).

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Secondary deformation during expansion and the leaf is not used. If the secondary folds are used for numerical refolding, the veins are drawn straight from one vein intersection to the next, and finally to a lobe tip. The anticalinal fold (or anti-veins) are drawn straight from the veins intersection to the sinus (lower point) of the perimeter (it is he same for primary and secondary anti-veins: anti-veins never connect to anything else than a vein meeting point, and a sinus). For the measurements (figures 8, 10, and 11), we used only the straight main veins and anti-veins, taking their length and separation angles. For the Data and Software, see below and the File S1.

Numerical Folding Method

Leaves are numerically folded back using the drawing of their veins (sincinal folds), contour and anti-veins (anticalinal folds, figure 13A). We first fold the main vein and anti-veins. They all join in the same point, at the end of the petiole. To refold the leaf, we just measure the angles between the successive veins and anti-veins (figure 13B), and redraw the leaf contour by inverting the sign of one angle on two, and correspondingly inverting the drawing of the contour piece. For instance, the piece of contour between the first vein and anti-vein is drawn inversed, with the vein horizontal. From the anti-vein, we then draw the next piece normally, between this anti-vein and the next vein. We then subtract the next angle, drawing the next vein/anti-vein piece inverted, add the next anti-vein/vein piece (figure 13C), and so on and so forth for the whole leaf (figure 13D).

To fold secondary folds there can be a geometrical problem. It is not always possible to keep the actual angles as resulting the folded sheet may not lie flat. The method used to numerically fold the leaves onto a plane keeps fold lengths and aims to keep at best the angle values between the folds. Finding close values is a way to project the folding into the plane (or look at it from the side), with minimal distortions. Lets consider the branching detail on figure 13E, sketched in figure 13F. When unfolded, a secondary fold is branching at a primary vein with an angle μ. The primary vein is making an angle α at this branching point. Between these two anticalinal folds, i.e., the secondary and the primary veins, stands a sincinal fold that makes angles α and β with them. To these angles α, β, μ and ν for the unfolded leaf, correspond the angles α', β', μ' and ν' when the leaf is folded (figure 13G).

The sum of these angles for the unfolded leaf is of course:

\[ α + β + ν + μ = 2π \]

Considering the angle ν', the sketch of figure 13G is in a plane only if:

\[ ν' = μ' − α' + β' \] (1)

If the sum of folded angles also follows (still on a plane unfolded)

\[ α' + β' + ν' + μ' = 2π \],

equation (1) rewrites:
\[(v' - v)^2 + (z' - 2)^2\]

which rewrites
\[(v' - v)^2 + (\pi - v' - 2)^2\].

One finds the best \(v'\) value:
\[v' = (\pi + v - 2) / 2\].

In the same way, one finds:
\[z' = (\pi + z - v) / 2,\]
\[\beta' = (\pi + \beta - \mu) / 2\] and
\[\mu' = (\pi + \mu - \beta) / 2\].

Once the angle corrected, the whole figure of folded veins and antiveins is drawn, and finally the contour is drawn for each vein-antivein segment, reverted if necessary, and with its angular position stretched or compressed if necessary, keeping the distance to the fold center (figure 13H). Usual corrections from the actual angles are around few degrees. For instance, in figure 6, the corrections are around 1.5°.

**Data and Software**

Data from the figures and software (in Matlab) are given as File S1. The data are the direct measurements of the positions of the petiole and main peaks and sinuses in many leaves, corresponding to figures 8, 10 and 11, together with the software allowing to extract the lengths and angles from them, and plot them as in the figures (folders: figure 8 and 10 – data; figure 11 – data). The Folding Software allows, once the contour of the image is obtained, and the information of the main and secondary veins and anti-veins obtained (via a sub-software), to fold back the contour. The cases form figures 6 and 9, with the original pictures, are provided as examples (folder: figure 6 and 9 - Folding and data). Short manuals are included.

**Formula**

Taking the sketch of figure 8A or figure 14, the condition that contour superimpose is:
\[\left(\bar{R}_a - \bar{R}_c\right)\wedge\left(\bar{R}_a - \bar{R}_b\right) = \bar{0}\]

which writes
\[-\bar{R}_a \wedge \bar{R}_b - \bar{R}_c \wedge \bar{R}_a + \bar{R}_b \wedge \bar{R}_c = \bar{0}\]

or
\[R_a R_c \sin(\pi - \beta) + R_a R_b \sin(\beta) = R_a R_b \sin(\pi)\].

This gives
Formula of figure 8D can be derived in the same way.

$$R_c = \frac{(R_a R_b \sin(\delta))}{(R_a \sin(\alpha - \beta) + R_b \sin(\beta))}$$

or similarly

$$R_c = \frac{(R_a \sin(\alpha))}{(R_a \sin(\alpha - \beta) + R_b \sin(\beta))}$$

Supporting Information

File S1 Data & Software
Found at: doi:10.1371/journal.pone.0007968.s001 (2.38 MB ZIP)

Author Contributions

Conceived and designed the experiments: EPLC SD. Performed the experiments: EPLC. Analyzed the data: EPLC SCdP SD. Wrote the paper: EPLC SCdP SD.
References

1. Nath U, Crasford BCW, Carpenter R, Coen E (2003) Genetic control of surface curvature. Science 299: 1404–1407.
2. Turing AM (1952) The chemical basis of morphogenesis. Phil Trans R Soc B 237: 37–72.
3. Thompson DAW (1942) On Growth and Form, 2nd edn Cambridge: Cambridge Univ. Press (2 t); Reprint: (1992) Dover. 1116 p.
4. Douady S, Couder Y (1996) Phyllotaxis as a self organizing process-Part I-II-III. J theor Biol 178: 255–312.
5. Arumí HJ, Guaschardena AN, Dengler NG (2006) Alternative modes of leaf dissection in monocotyledons. Bot J Linn Soc 150: 25–44.
6. Hagemann W, Glensberg S (1996) Organogenetic capacity of leaves: the significance of marginal blastozones in angiosperms. Plant Systemat Evol 199: 121–152.
7. Franks NR, Britton NF (2000) The possible role of reaction-diffusion in leaf shape. Proc R Soc Lond B 267: 1295–1300.
8. Marder M, Sharon E, Roman B, Smith S (2003) Theory of the edge of leaves. EPL 62: 498–504.
9. Melville R, Wrigley FA (1969) Fenestration in the leaves of Monstera and its bearing on the morphogenesis and colour patterns of leaves. Bot J Linn Soc 62: 1–16.
10. Kaplan DR, Dengler NG, Dengler RE (1982) The mechanism of plication inception in palm leaves: problem and developmental morphology. Can J Bot 60: 2939–2973.
11. Boudaoud A, Patricio P, Couder Y, Ben Amar M (2000) Dynamics of singularities in a constrained elastic plate. Nature 407: 718–720.
12. Mahadevan L, Rica S (2005) Self-organized origami, Science 307: 1740.
13. Kobayashi H, Kiesling B, Vincent JFV (1998) The geometry of unfolding tree leaves. Proc R Soc Lond B 265: 147–154.
14. Adanson M (1763) Familles des plantes: contenant une préface historique sur l’état ancien et actuel de la botanique, et une théorie de cette science. Paris: Chez Vincent imprimeur du Comte de Provence. (ccli-cclii), 2 t, 660 p. Reprint (1966): Stuttgart: J. Cramer. (210-212) 297 p.
15. Cloos D (1870) Monographie de la préfoliation, dans ses rapports avec les divers degrés de classification. Toulouse: Rouget frères et Delahaut. 48 p.
16. Demaine ED, Demaine ML, Lauben A (1998) Folding and One Straight Cut Suffice. Proceedings of the 10th Annual ACM-SIAM Symposium on Discrete Algorithms, pp 891–892.
17. Angiosperm Phylogeny Group (2003) An update of the Angiosperm Phylogeny Group classification for the orders and families of flowering plants: APG II. Bot J Linn Soc 141: 399–436.
18. Bharathan G, Goliber TE, Moore C, Kreider S, Pham T, et al. (2002) Homologies in Leaf Form Inferred from KNOXI Gene Expression During Development. Science 296: 1858–1860.
19. Blein T, Palasso A, Vialato-Guion-Aud, Nikowits K, Merin H, et al. (2008) A Conserved Molecular Framework for Compound Leaf Development. Science 322: 1835–1839.
20. Braam J (2005) In touch: plant responses to mechanical stimuli. New Phytologist 165: 373–389.
21. Scarpella E, Marcos D, Friml J, Berleth T (2006) Control of leaf vascular patterning by polar auxin transport. Genes Dev 20: 1015–1027.
22. Bailey IW, Sinott EW (1916) The climatic distribution of certain type of angiosperm leaves. Am J Bot 60: 24–39.
23. Rolland-Lagan AG, Bangham AJ, Coen E (2003) Growth dynamics underlying petal shape and asymmetry. Nature 422: 161–163.