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A hint on the metal-free star formation rate density from 21-cm-EDGES data

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ABSTRACT
We aim to provide here the first data-constrained estimate of the metal-free (Population III; Pop III) star formation rate density $\dot{\rho}^{III}\text{}_\star$ required at high redshifts ($z \sim 16$) in order to reproduce both the amplitude and the redshift of the EDGES 21-cm global signal. Our model accounts for the Ly $\alpha$, radio, and X-ray backgrounds from both Pop III and metal-enriched Population II (Pop II) stars. For the latter, we use the star formation rate density estimates (and the Ly $\alpha$ background) from the Delphi semi-analytic model that has been shown to reproduce all key observables for galaxies at $z \sim 5$; the radio and X-ray backgrounds are fixed using low-$z$ values. The constraints on the free parameters characterizing the properties of the Pop III stars are obtained using a Markov Chain Monte Carlo analysis. Our results yield a $\dot{\rho}^{III}\text{}_\star$ that while increasing from $z \sim 21$ to 16 thereafter shows a sharp decline which is in excellent agreement with the results found by Valiante et al. to simulate the growth of $z \sim 6$–7 quasars and their host galaxies, suggesting that the bulk of Pop III star formation occurs in the rarest and most massive metal-poor haloes at $z \lesssim 20$. This allows Pop III stars to produce a rapidly growing Ly $\alpha$ background between $z \sim 21$ and 15. Further, Pop III stars are required to provide a radio background that is about 3–4 orders of magnitude higher than that provided by Pop II stars although Pop II stars dominate the X-ray background.

Key words: stars: Population II – stars: Population III – galaxies: high-redshift – intergalactic medium – dark ages, reionization, first stars.

1 INTRODUCTION
The past few years have seen enormous advances in peering back to the era of early star formation (for a recent review see Dayal & Ferrara 2018), with instruments such as the Hubble Space Telescope proving glimpses of star formation at redshifts as high as $z \sim 11$ (Oesch et al. 2016) with a resolution of a few parsecs (e.g. Bouwens et al. 2017; Vanzella et al. 2019). However, the first metal-free (Population III; Pop III) stars postulated to explain the metallicity gap from big bang nucleosynthesis to the metal-rich (Population II; Pop II) stars seen in high-redshift galaxies or in the low-metallicity tail of the metallicity distribution function of Galactic halo stars remain elusive. The fact that the first stars lasted only a few Myr, if their initial mass function is pre-dominantly top-heavy (see Bromm 2013 for a thorough review) coupled with their predicted low star formation efficiency (Tornatore, Ferrara & Schneider 2007; Maio et al. 2010, 2011; Johnson, Dalla Vecchia & Khochfar 2013; Xu et al. 2016; de Bennassuti et al. 2017; Jaacks et al. 2018; Sarmento, Scannapieco & Côté 2019), has, so far, not resulted in the detection of any metal-free stars at high-$z$ (see however Vanzella et al. 2020 for a strongly lensed candidate Pop III star complex at $z = 6.6$). Indeed, models require an instantaneous Pop III burst of $\sim 10^5 M_\odot$ for such first stars to be visible with the James Webb Space Telescope (e.g. Zachrisson et al. 2015).

However, recently, another avenue has opened up with regard to studying star formation at extremely high redshifts ($z \sim 16$). This is the result provided by the EDGES (Experiment to Detect the Global Epoch of Reionization Signature) collaboration (Bowman et al. 2018). These authors have measured a sky-averaged 21-cm absorption signal (from neutral hydrogen) at a central frequency $\nu = 78 \pm 1$ MHz corresponding to $z \approx 17.2$. While this redshift is consistent with expectations of Ly $\alpha$ photons coupling the spin temperature of neutral hydrogen to the gas kinetic temperature in
the standard cold dark matter paradigm, the differential brightness temperature $-500 \pm 200 \text{ mK}$ is about twice as strong as that expected from any ‘standard’ model (Barkana 2018). Explaining the strength of this signal either requires gas colder than expected or a radiation background higher than expected (Bowman et al. 2018).

Indeed, given its possible origin from within the first 250 Myr of the Universe, this signal has already been proposed to test new dark matter physics (Barkana 2018; Fraser et al. 2018; Pospelov et al. 2018; Slatyer & Wu 2018; Chatterjee et al. 2019). On the other hand, the excess radio background solution (Feng & Holder 2018; Fialkov & Barkana 2019) could point to populations of early black holes/micro-quasars (Ewall-Wice et al. 2018; Mirabel 2019), Pop III stars (Jana, Nath & Biermann 2019; Schauer, Liu & Bromm 2019), or extremely efficient star formation in low-mass haloes (Mirocha & Furlanetto 2019).

In this work, we carry out a proof-of-concept calculation assuming that the EDGES signal is driven by a combination of Pop II and Pop III stars. Our aim is to provide the first data-constrained estimate of the star formation rate density (SFRD) at such high-$z$, using a Markov Chain Monte Carlo (MCMC) approach, which results in a 21-cm signal at the right redshift with an amplitude and shape compatible with the EDGES result.

The cosmological parameters used in this work correspond to $\Omega_m = 0.3089$, $\Omega_b = 0.6911$, $\Omega_\gamma = 0.049$, $h = 0.67$, $n_s = 0.96$, and $\sigma_8 = 0.81$ (Planck Collaboration 2016).

2 THEORETICAL MODEL

The observable in global 21-cm experiments like EDGES is the globally averaged differential brightness temperature which, for the cosmological parameters used in this work, is given by (Chatterjee et al. 2019)

$$\delta T_b(v) = 10.1 \text{ mK} \chi_{\text{HI}}(z) \left( 1 - \frac{T_s(z)}{T_\gamma(z)} \right) (1+z)^{1/2},$$

where $v$ is the frequency of observation, $\chi_{\text{HI}}$ is the neutral hydrogen fraction, $T_s$ is the spin temperature which includes the cosmic microwave background (CMB) plus a radio background, if any, and $T_\gamma$ is the spin temperature of neutral hydrogen. In the above, we have assumed the intergalactic medium (IGM) to be predominantly neutral at redshifts corresponding to the EDGES observations.

We calculate the differential brightness temperature using the theoretical model detailed in Chatterjee et al. (2019) which closely follows that of Furlanetto, Oh & Briggs (2006b) and Pritchard & Loeb (2012). In brief, the spin temperature can be written as (Field 1958)

$$T_s^{-1} = T_\gamma^{-1} + x_e T_k^{-1} + x_h T_u^{-1},$$

where $T_k$ is the gas kinetic temperature and $T_u$ is the colour temperature of the Ly$\alpha$ radiation field. Further, $x_e$ and $x_h$ are the coupling coefficients corresponding to collisional excitations and spin-flip due to the Ly$\alpha$ radiation field, respectively. In this work, we assume $T_u = T_k$. This is justified by the fact that the high optical depth for Ly$\alpha$ photons ensures that they undergo a large number of scatterings which are sufficient to bring the Ly$\alpha$ radiation field and the gas into local equilibrium near the central frequency of Ly$\alpha$ radiation (Pritchard & Loeb 2012).

We start by describing our calculation of the coupling coefficients before discussing the kinetic temperature in equation (2). The collisional coupling coefficient, $x_c$, is determined by three different channels, namely, hydrogen–hydrogen (H–H), hydrogen–electron (H–e), and hydrogen–proton (H–p) collisions.

Though the collisional coefficients do not play any important role at epochs relevant to this work we include them in our numerical code for completeness.

The Ly$\alpha$ coupling coefficient, $x_c$, is determined by the background Ly$\alpha$ flux, $J_{\alpha}$, as

$$x_c = \frac{1.81 \times 10^{11}}{(1+z)} S_d \frac{J_{\alpha}}{\text{cm}^{-2} \text{s}^{-1} \text{Hz}^{-1} \text{sr}^{-1}},$$

where $S_d$ is a factor of order unity that accounts for the detailed atomic physics involved in the scattering process (Furlanetto, Oh & Pierpaoli 2006a; Hirata 2006). We calculate the total background Ly$\alpha$ flux at redshift $z$, accounting for the contribution from both Pop II and Pop III stars, as

$$J_{\alpha}(z) = \frac{c}{4\pi} (1+z)^3 \int_1^{\alpha_{\max}} \frac{d\nu'}{dz'} d\nu'. \quad (4)$$

Here $\nu' = \nu_d (1+z)/(1+z)$, $\nu_d$ is the Ly$\alpha$ frequency, $\alpha_{\max}$ is the production rate of Ly$\alpha$ photons per unit frequency per unit comoving volume at redshift $z$ which effectively scales with the SFRD, $c$ is the speed of light, and $f$ is the cosmic time corresponding to the redshift $z$. The upper limit of the integral corresponds to $\nu' = \nu_{\text{LL}}$, i.e.

$$1 + z_{\text{LL}} = \frac{\nu_{\text{LL}} (1+z)}{c},$$

where $\nu_{\text{LL}}$ is the frequency corresponding to the Lyman limit. Note that this upper limit implies that $J_{\alpha}$ does not contain any contribution from ionizing photons $\nu \geq \nu_{\text{LL}}$ as they will be absorbed by neutral hydrogen atoms. For both Pop II and Pop III stars, we make the assumptions that all photons with $\nu_d < \nu < \nu_{\text{LL}}$ escape the host galaxy (since they avoid resonant scattering with neutral atoms) and that the spectrum of photons around the Ly$\alpha$ frequencies is constant (Furlanetto et al. 2006a).

For Pop II stars, the rate $\rho_{\alpha}^{\text{HII}}(z)$ is directly obtained from the Delphi semi-analytic model. This value is obtained based on the entire assembly history of a galaxy using the Starburst99 stellar population synthesis model (Leitherer et al. 1999) assuming a constant metallicity value of 5 per cent $Z_\odot$ and assuming each newly formed stellar population to have an age of 2 Myr. For simplicity, for Pop III stars, we assume $\rho_{\alpha}^{\text{HII}}(z)$ to be proportional to the corresponding SFRD $\rho_{\alpha}^{\text{HII}}(z)$ such that

$$\frac{\rho_{\alpha}^{\text{HII}}(z)}{\text{Mpc}^{-3} \text{yr}^{-1}} = \frac{J_{\alpha}^{\text{HI}}}{\text{Hz}^{-1}} \frac{\rho_*^{\text{HII}}(z)}{\text{M}_\odot \text{Mpc}^{-3} \text{yr}^{-1}},$$

where $f_{\alpha}^{\text{HI}}$ is a proportionality factor that is treated as a free parameter and fixed using observations.

The gas kinetic temperature is determined by three processes: (i) the adiabatic cooling because of the expansion of the Universe, (ii) heating/cooling due to Compton scattering of residual electrons with background photons assuming an ionization fraction $\geq 10^{-4}$; Bharadwaj & Ali 2004), and (iii) X-ray heating/cooling. For this process, the globally averaged energy injection rate per unit volume is taken to be proportional to the corresponding SFRD ($\rho_*$) as

$$\frac{\epsilon_x}{\text{J Mpc}^{-3} \text{s}^{-1}} = 3.4 \times 10^{33} \left( f_{\text{X},h}^{\text{II}} \rho_*^{\text{HII}}(z) + f_{\text{X},h}^{\text{III}} \rho_*^{\text{HIII}}(z) \right) \text{M}_\odot \text{Mpc}^{-3} \text{yr}^{-1},$$

where the proportionality factor $f_{\text{X},h} = f_X \times f_n$, where $f_X$ is an unknown normalization factor allowing one to account for differences.
between the scaling obtained from local observations and that at high-z, and \( f_R \) is the fraction of the X-rays that contribute to heating (the other part goes into ionization). The superscripts denote the contributions of Pop II and Pop III stars. For Pop II stars, we assume that the scaling between the X-ray luminosity and the star formation rate remains unchanged as compared to low-z observations and set \( f_R^{\text{II}} = 1 \). We also assume \( f_R^{\text{II}} = 0.2 \), appropriate for the early stages of reionization (Furlanetto et al. 2006b). These assumptions fix the value of \( f_R^{\text{II}} \) for Pop III stars, we leave \( f_R^{\text{III}} \) as a free parameter.

It has now been well established that in order to match the amplitude of the EDGES signal we would either require making the gas colder, using exotic physics such as new dark matter interactions (Barkana 2018; Fraser et al. 2018; Pospelov et al. 2018; Slatyer & Wu 2018) or invoking a radiation temperature larger than the CMB temperature (Fraser et al. 2018; Pospelov et al. 2018; Ewall-Wice et al. 2018; Feng & Holder 2018; Jana et al. 2019). In this work, we avoid incorporating any non-standard physics and focus on the latter scenario, as it has got some support by observations of an excess radio background in the local Universe, reported by the ARCADE-2 experiment (Fixsen et al. 2011). We model the excess radio background by assuming that early galaxies produce radio frequency radiation whose strength is proportional to the star formation rate. The local radio-star formation rate (\( L_R / M_\odot \text{ yr}^{-1} \)) relation at 150 MHz is given by (Gürkan et al. 2018)

\[
\frac{L_R}{J \text{s}^{-1} \text{Hz}^{-1} \text{Mpc}^{-3}} = 10^{22} \left( \frac{M_\odot \text{ yr}^{-1}}{M_\odot \text{ yr}^{-1}} \right) \left( \frac{\text{Hz}}{1000} \right). \tag{8}
\]

We assume that a similar scaling holds at high redshifts too and hence the globally averaged radio luminosity per unit comoving volume (i.e. the radio emissivity) is given by

\[
\epsilon_R(z) \left( \frac{J \text{s}^{-1} \text{Hz}^{-1} \text{Mpc}^{-3}}{10^{22}} \right) = 10^{22} \left( \frac{f_R^{\text{II}}}{M_\odot \text{ yr}^{-1}} \right) \left( \frac{\text{Hz}}{1000} \right) \left( \frac{\text{Hz}}{1000} \right) \left( \frac{\text{Hz}}{1000} \right), \tag{9}
\]

where \( f_R \) accounts for any differences between the local observations and high-z; we use \( f_R^{\text{II}} = 1 \). The emissivity can be extrapolated from 150 MHz to higher frequencies by assuming a radio spectral index \( \alpha_R \). The 21-cm radiation flux can then be written as (Ciardi & Madau 2003)

\[
F_R(z) = \left( \frac{1420}{150} \right) \frac{\epsilon_R(1+z)}{4\pi} z \int_z^\infty \epsilon_{R,\nu}(z') \frac{dz'}{z^2}, \tag{10}
\]

where \( \epsilon_{R,\nu}(z') \) is the comoving radio emissivity at \( \nu' = 150 \text{ MHz} (1 + z) / (1 + z) \) and the factor \((1420/150)^{\alpha_R}\) on the right-hand side accounts for the frequency dependence of the radio emissivity. In this work, we assume \( \alpha_R = -0.7 \) (Gürkan et al. 2018). Using the Rayleigh–Jeans law, the flux can be converted into a radio brightness temperature \( T_R \), which results in a total background temperature given by \( T_R(z) = T_{R,\nu}(z) + T_{\text{CMB}}(z) \).

As seen from this discussion, the only z-dependent quantities entering the equations explicitly are the SFRDs for Pop II and Pop III stars. As already noted, for Pop II stars we use the SFRD and Ly\( \alpha \) photon production rate results from the Delphi semi-analytic model that has been shown to reproduce all key observables for galaxies and active galactic nuclei (AGNs; including their UV luminosity functions, stellar mass/black hole mass densities, SFRDs, the stellar/black hole mass function) at \( z \gtrsim 5 \) (Dayal et al. 2014, 2019). From this model, we find that the redshift evolution of the Pop II SFRD is well described by log(\( \rho_{\text{II}}^z / M_\odot \text{ Mpc}^{-3} \text{ yr}^{-1} \)) = \(-0.008(1 + z)^2 + 0.047(1 + z) - 0.995 \).

As for Pop III stars, we parametrize \( \rho_{\text{III}}^z(z) \) as function of redshift and attempt to constrain its shape using the EDGES observations. Note that the three essential physical quantities \( n_e, T_h, \) and \( f_R (\text{or } T_{X,h}) \) that determine the observable \( S_T(z) \) depend on the Pop III SFRD only through the combinations \( f_{\text{II}}^{\text{II}}, f_R^{\text{II}}, f_{\text{III}}^{\text{II}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}} \), respectively. Hence the overall normalization of \( \rho_{\text{III}}^z(z) \) is completely degenerate with the free parameters \( f_{\text{II}}^{\text{II}}, f_R^{\text{II}}, f_{\text{III}}^{\text{II}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}} \). In view of this, we parametrize the Pop III SFRD using the log–polynomial form

\[
\log \left[ \frac{\rho_{\text{III}}^z(z)}{\rho_{\text{III}}^z(z_{\text{mean}})} \right] = \sum_{i=1}^{4} a_i (z - z_{\text{mean}})^i
\]

where \( a_1, a_2, a_3, a_4 \) are free parameters and \( z_{\text{mean}} = 17.15 \) is the mean redshift of the EDGES observations. We find that parametrization of \( \rho_{\text{III}}^z(z) \) using a smaller number of parameters does not allow any good fit to the data, while using more terms in the polynomial leads to strong degeneracies between the coefficients. In order to simplify the problem, we use normalization such that \( \rho_{\text{III}}^z(z_{\text{mean}}) = 10^{-4.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3} \) which is motivated by the simulation results of Valiante et al. (2016). Note that this choice of the normalization has no impact on the constraints we obtain on the redshift dependence of \( n_e, T_h, \) and \( f_R (\text{or } T_{X,h}) \) and the subsequent conclusions; all that would change when varying \( \rho_{\text{III}}^z(z_{\text{mean}}) \) would be the amplitude of the coefficients \( f_{\text{II}}^{\text{II}}, f_R^{\text{II}}, f_{\text{III}}^{\text{II}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}}, f_{\text{III}}^{\text{III}} \). We reiterate that, in our approach, the modelling of the Pop III SFRD is completely free of any physical assumptions and the form is solely constrained using data.

To summarize, our model has a total of seven free parameters: four for the Pop III SFRD (\( a_1 - a_4 \)) and three for the temperature contribution for Pop III stars (\( f_R^{\text{II}}, f_R^{\text{II}}, f_{\text{III}}^{\text{II}} \)). Additionally, we have assumed \( f_R^{\text{II}} = 1 \) and \( f_R^{\text{II}} = 0.2 \). Finally, while the value of \( \rho_{\text{III}}^z(z_{\text{mean}}) \) is obtained from the Delphi semi-analytic model, we use a normalization of \( \rho_{\text{III}}^z(z_{\text{mean}}) = 10^{-4.5} M_\odot \text{ yr}^{-1} \text{ Mpc}^{-3} \).

By comparing the predictions of our model with EDGES data, we constrain the values of these parameters and consequently study the implications of the Pop III star formation at high-z. The constraints on the parameters, i.e. their posterior probability distributions are computed using a Bayesian statistical method based on MCMC. We make use of the publicly available emcee package (Foreman-Mackey et al. 2013) for this purpose.

The MCMC analysis requires computing a likelihood \( L \propto e^{-L/2} \), with the usual definition of the chi-square error such that

\[
L = \sum_i \frac{\left[ \delta T_{\text{model}}(v_i) - \delta T_{\text{data}}(v_i) \right]^2}{\sigma_i}, \tag{12}
\]

where the sum is over all frequency bins corresponding to the EDGES data and \( \sigma_i \) is the error. We take \( \sigma_i = 25 \text{ km s}^{-1} \), consistent with Hills et al. (2018). We assume all the seven parameters to have broad flat priors: the priors for \( a_1, a_2, a_3, a_4 \) span the whole range from \(-\infty \) to \( \infty \) whereas \( f_{\text{II}}^{\text{II}}, f_R^{\text{II}}, f_{\text{III}}^{\text{II}} \) are allowed to vary between 0 to 10. For exploring the parameter space with MCMC chains, we make use of 96 walkers taking \( 1.5 \times 10^5 \) steps. The initial 25 per cent steps are removed as ‘burn-in’ and the remaining ones

1Essentially, walkers are the members of the ensemble that sample the posterior probability distribution function. They are similar to the popularly
are used for estimating the posterior distributions. We have carried out the auto-correlation analysis (Goodman & Weare 2010) of the chains to ensure that the distributions have converged.

3 RESULTS

As already shown in Chatterjee et al. (2019), simultaneously matching to the shape and amplitude of the EDGES signal requires an Ly α background already in place by z ∼ 20 that can couple the spin temperature to the gas temperature, an excess radio background at z ∼ 20 that yields a signal of the depth required and that falls off steeply at z ∼ 17, and an X-ray background by z ∼ 17 that heats the gas so as to reduce the absorption amplitude.

We start by quantifying the 1-D and 2-D projections of the posterior probability distributions of all the seven Pop III free-parameter values required to yield these trends in Fig. 1. First, the increasing Pop III SFRD values at z > z_{\text{mean}} are essentially driven by the positive \(a_1(z - z_{\text{mean}})\) term; the remaining three terms (with coefficients \(a_2\), \(a_3\), and \(a_4\) in equation (1)) are responsible for the steep downturn seen at z ∼ 16. Moving to the fourth row of the same figure, we find \(f_{\alpha}^{\text{III}} \sim 200 \times 10^{25}\). As seen in what follows, this results in a situation where Pop III stars dominate the Ly α background between z ∼ 21 – 15. Further, as seen from these plots, per unit SFRD, Pop III stars are required to provide a radio background that is about 400 times higher than that provided by Pop II stars (where \(f_{\alpha}^{\text{II}} = 1\)), assuming the normalization \(\rho_{\text{III}}(z_{\text{mean}}) = 4 \times 10^{-4.5} \, \text{M}_\odot \, \text{yr}^{-1} \, \text{Mpc}^{-3}\). This naturally results in a radio background that is predominantly driven by Pop III stars. Indeed, this is the key factor that determines the fall-off of the Pop III SFRD. Finally, we find that Pop II stars dominate the X-ray background at all z with Pop III stars providing almost no contribution. This is required to maintain the spin temperature being coupled to the gas temperature between z ∼ 16 and 19 and yield the EDGES absorption trough. Indeed, the earlier the X-ray background arises, the faster the spin temperature saturates to the CMB temperature.

Next, we focus on analysing the contribution of Pop II and Pop III stars to the EDGES signal, as shown in Fig. 2. In addition to the best-fitting values for Pop II, we also show results for 1000 random points sampled from the chains; the region spanned by these sampled curves should be thought of as the range of histories that are allowed by the EDGES data. From panel (a), we see that our model results are in reasonable agreement with the EDGES data with the match being particularly good at z ∼ 16. We find that the match degrades at z ∼ 16 where our models evolve somewhat slower than what is required by the data. This part of the evolution is driven by X-ray heating from Pop II stars, which in turn is fixed by the Delphi output; a better match would require steeper evolution in the Pop II star formation rate.

Panel (b) in the same figure shows the Pop III SFRD which is always subdominant compared to the Pop II stars. This is mainly because of the normalization we have chosen. However, as noted before, our key results concern the shape of the Pop III SFRD. The data requires a rise in Pop III stars at z ∼ 20–21 followed by a sharp fall at z ∼ 15–16. The evolution of \(f_{\alpha}^{\text{III}}(z)\) also shows a ‘kink’-like feature at z ∼ 18 which is due to a similar feature in the absorption profile as observed by EDGES. This is only to be expected - since our model of Pop III stars is entirely driven by data, any feature present in the data would show up in the model predictions as well.

In panel (d), we see that the Ly α emissivity is completely dominated by Pop III stars at redshifts relevant for the EDGES observations. Note that, unlike \(\rho_{\text{III}}^{\text{III}}(z)\), this emissivity does not depend on the normalization; this is because as seen from equation (6), the emissivity depends on the product of \(\rho_{\text{III}}^{\text{III}}(z)\) and \(f_{\alpha}^{\text{III}}(z)\) which absorb all the uncertainties. On the other hand, the X-ray emissivity from Pop III stars is always subdominant compared to the Pop II stars. This implies that the amount of heating required to match the EDGES data can be contributed solely by the Pop II stars (as modelled in Delphi). Indeed, a larger contribution from Pop III stars would lead to a faster coupling between the spin and CMB temperatures, resulting in a higher redshift at which the signal would tend to 0. Finally, in all panels, we also show by the grey shaded regions the models that are consistent with the EDGES data. As expected, while the range of histories naturally shows a dispersion, their redshift-evolution remains unaffected. The Pop III SFRD and the radio emissivity show the least dispersion (since they effectively govern the brightness temperature from Pop III stars) while, given their negligible contribution to the X-ray emissivity, the value of \(\dot{f}_{X}^{\text{III}}\) shows the largest dispersion.

It is worth pointing out here that the depth of the EDGES signal is highly controversial (see, e.g. Hills et al. 2018; Sims & Pober 2020). In case the amplitude of the signal turns out to be much smaller than what is assumed in this work (say |ΔT_s| < 100 mK), then the Pop II stars with conventional choice of efficiency parameters are sufficient to explain the observations. Hence our conclusions on the Pop III stars hold only in the case where the amplitude and redshift extent of the 21-cm signal are similar to those reported by the EDGES experiment.

Finally, we compare our predicted redshift evolution of the Pop III SFRD with some theoretical models in Fig. 3. Most models predict a Pop III SFRD that either rises between z ∼ 22 and 13 (Jaacks et al. 2018; Sarmento et al. 2019) or shows a relatively constant behaviour for z ∼ 20 – 13 (Johnson et al. 2013). The only exceptions are the predictions by Valiante et al. (2016), Valiante et al. (2018), whose amplitude and redshift dependence are very similar to our predicted shape. Interestingly, the Valiante et al. (2016), Valiante et al. (2018) models aim to describe the formation histories of z ∼ 6–7 quasars and their host galaxies. They therefore describe rapidly evolving and biased regions of the Universe. In these models, Pop III stars (and their black hole remnants) start to form at z > 20 in dark matter mini-haloes with mass \(10^{8.4} M_\odot\). However, their formation efficiency is small, as Lyman-Werner radiation limits gas cooling due to H_2 photo-dissociation. Because of this, the bulk of Pop III stars form at redshift 15 < z < 20 in metal poor (Z < Z_\odot = 10^{-3.8} Z_\odot) Ly α-cooling haloes, with mass \(10^{7.5} - 10^{8.5} M_\odot\) that are able to self-shield and cool the gas more efficiently (see the top panel of Fig. 1 in Valiante et al. 2018). At z ≤ 15 Pop III star formation is suppressed by metal enrichment, as Z < Z_\odot = 10^{-3.8} Z_\odot star forming regions become increasingly rare. Hence, the shape of the EDGES signal suggests that the rapid coupling between the spin temperature and the gas kinetic temperature is driven by Ly α photons produced by Pop III stars that form in relatively massive and rare haloes, whose abundance grows fast, due to the exponential growth of the massive-end of the halo mass function, before the quick rise of the gas temperature rapidly erases the signal at z ∼ 16. Interestingly, these considerations are very
consistent with the results of Kaurov et al. (2018), who also suggest that the shape of the EDGES signal can be best explained if the bulk of the UV photons are produced by rare and massive haloes, and explore the implications for the amplitude of the 21-cm power spectrum.

4 CONCLUSIONS AND DISCUSSION

In this work, we aim to provide an estimate of the Pop III SFRD required at high redshifts ($z \gtrsim 16$) in order to reproduce both the amplitude and the redshift of the EDGES 21-cm global signal. This essentially requires a rapidly rising Ly$\alpha$ background at $z \sim 20$ (to couple the spin temperature to the gas temperature), an excess radio background at $z \sim 20$ that falls off steeply at $z < \sim 17$ (to match to the depth and subsequent increase of the EDGES signal), and an X-ray background by $z \sim 17$ (to heat the gas so as to reduce the absorption amplitude). Our model has a total of seven free parameters: four for the Pop III SFRD ($a_1$–$a_4$) and three for the temperature contribution for Pop III stars ($f_{X, h}^{III}$, $f_R^{III}$, $f_{\alpha}^{III}$); we use a normalization of $\rho_{III}^*(z_{\text{mean}}) = 10^{-4.5} \, M_\odot \, \text{yr}^{-1} \, \text{Mpc}^{-3}$.
Figure 2. As a function of redshift, the panels show the results for Pop II stars and Pop III stars for models that fit the EDGES brightness temperature for: (a) the differential brightness temperature where the blue points show the EDGES data, (b) the star formation rate densities, (c) the radio emissivity, (d) the Ly \( \alpha \) photon production rate, and (e) the X-ray emissivity. We artificially force the Pop II SFRD to be zero at \( z > 19.5 \) because the formation of Pop II stars cannot precede that of Pop III stars. In all panels, the green and red lines show the results for Pop II (based on Delphi) and Pop III stars (the best-fitting model obtained from MCMC) respectively. The grey shaded regions show 1000 random samples from the joint posterior distribution, i.e. they represent models that are consistent with the EDGES data.

Figure 3. The redshift evolution of the Pop III star formation rate density. The black line (best-fitting model from this work) is compared to other theoretical estimates from Johnson et al. (2013, dashed purple line), Jaacks et al. (2018, dot–dashed blue line), and Sarmento et al. (2019, solid green line). Finally, the thin red lines show the results for 10 different simulations by Valiante et al. (2016), which aim to reproduce the observed properties of \( z \sim 6–7 \) quasars and their host galaxies (see the text).

motivated by simulation results of Valiante et al. (2016). These seven parameters are constrained using the emcee package, a Bayesian statistical method based on MCMC. As for Pop II stars, the SFRD and Ly \( \alpha \) photon production rate are obtained directly from the Delphi semi-analytic model that has been shown to reproduce all key observables for galaxies and AGNs at \( z \sim 5 \) (Dayal et al. 2014, 2019). Finally, we use \( f_{\text{II}}^R = 1 \) and \( f_{\text{X,II}}^R = 0.2 \) in order to be consistent with low-redshift observations. This results in a first estimate of the redshift evolution of the Pop III SFRD whose form is solely constrained using data. Our key results are:

(i) Our model predicts a Pop III SFRD that while increasing from \( z \sim 21 \) to 16 thereafter show a sharp decline. While this is in excellent agreement with the results of Valiante et al. (2016, 2018), there is a disparity with the results of most other models that predict a Pop III SFRD that either rises between \( z \sim 22 \) and 13 (Jaacks et al. 2018; Sarmento et al. 2019) or shows a relatively constant behaviour for \( z \sim 20–13 \) (Johnson et al. 2013).

(ii) Pop III stars dominate the Ly \( \alpha \) background between \( z \sim 21 \) and 15.

(iii) Pop III stars are required to provide a radio background that is about 3–4 orders of magnitude higher than that provided by Pop II stars, resulting in a radio background that is predominantly driven by Pop III stars.

(iv) Pop II stars dominate the X-ray background at all \( z \) (where \( f_{\text{X,II}}^R \sim 0.2 \) with Pop III stars providing almost no contribution. The above findings suggest that the rapidly rising Ly \( \alpha \) background implied by the EDGES signal is dominated by the emission of Pop III stars formed in metal-poor Ly \( \alpha \)-cooling haloes with mass \( 10^{7.5}–10^{8.5} \) M\(_{\odot}\) (Valiante et al. 2016, 2018). These systems are massive enough to provide a rapidly growing contribution at \( z \sim 21–19 \), due to the exponential growth of the massive end of the halo mass function (see also Kaurow et al. 2018), but their number is large enough to ensure that the spin temperature and the gas kinetic temperature are coupled in a large fraction of the...
Universe. In an earlier work, Mebane, Mirocha & Furlanetto (2020) have studied the effects of Pop III remnants on the 21-cm signal and compared their results with the EDGES data. Analogous to this work, they have also found that the subset of their Pop III SFRD models that are able to match the timing and position of depth of the EDGES signal always prefer larger radio emission and small X-ray emission. In another recent (similar) work, using a more physically motivated model of Pop III stars, Schauer et al. (2019) find that Pop III stars are crucial in providing the necessary Ly $\alpha$ flux at high redshifts in order to agree with the EDGES data, consistent with our conclusions regarding the Ly $\alpha$ flux.

We should also mention that our galaxy formation model (Delphi) and also the quantities $f^2_\alpha$ and $f^2_{\text{ IDs}}$ for Pop II stars are calibrated to lower redshift observations and could be different at higher redshift. However, in the absence of any rigorous model or observation at high redshifts, we have taken the most conservative approach and kept the values of these parameters constant. This also ensures that the number of free parameters does not increase beyond control.

However, the question that remains is: how can Pop III stars dominate the Ly $\alpha$ and radio backgrounds and be completely subdominant for the X-ray background? Pop III stars can give rise to a radio background as a result of synchrotron emission from high-energy cosmic ray (CR) electrons accelerated in SN explosions, but the signal is accompanied by substantial IGM heating due to CR protons (Jana et al. 2019). Hence, even without including the effect of X-ray heating, the associated CR proton heating limits the contribution of Pop III SNe to the radio background required to explain the depth of the absorption trough in the EDGES signal, unless the ratio of the CR electrons to protons energy is substantially larger than usually assumed. An additional contribution to the radio background at cosmic dawn could come from accreting black hole remnants of Pop III stars. Again, to avoid the associated X-ray heating of the IGM, the X-rays must be absorbed by a substantial column of gas, with $N_{\text{HI}} \sim 5 \times 10^{21}$ cm$^{-2}$, for $\sim 100$ Myr (Ewall-Wice et al. 2018). This requirement allows to have escape fractions of ionizing photons $f_{\text{esc}} \sim 0$ to avoid exceeding the Planck constraint on the Thompson scattering optical depth (Planck Collaboration 2016) and boosting-up the emission of Ly $\alpha$ photons.

Whatever the true physical explanation is, it is clear that the shape of the 21-cm signal measured by EDGES has offered a first glimpse on the potential of 21-cm observations to constrain the properties of the Universe at cosmic dawn.

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3Following Kaurow et al. (2018), the light travel distance between $z = 21$ and $z = 19$ can be estimated as $113$ h$^{-1}$ Mpc and the number density of the sources has to be $\geq 10^{-6.8}$ (h$^{-1}$ Mpc$^{-3}$), that is satisfied if the sources reside in haloes with $\geq 10^{9.7}$ M$_{\odot}$.
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