LETTER TO THE EDITOR

Magnitude and direction of the local interstellar magnetic field inferred from Voyager 1 and 2 interstellar data and global heliospheric model

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ABSTRACT

In this Letter, we provide constraints on the direction and magnitude of the pristine (i.e., unperturbed by the interaction with the Sun) local interstellar magnetic field. The constraints are based on analysis of the interstellar magnetic field components at the heliopause measured by magnetometer instruments on board Voyager 1 and 2 spacecraft. The analysis was performed with the help of our kinetic-magnetohydrodynamical model of the global heliosphere. The model shows that the solar-induced disturbances of the interstellar magnetic field are extended relatively far from the Sun up to 400–500 AU. The field is draped around the heliopause and compressed. By comparison of the model results with Voyager data we found that the model provides results comparable with the data for the interstellar magnetic field of $B_{\text{LISM}} \approx 3.7-3.8 \mu G$ in magnitude and directed towards $\approx 125^\circ$ in longitude, and $\approx 37^\circ$ in latitude in the heliographic inertial coordinate system.

Key words. Sun: heliosphere – solar wind – ISM: magnetic fields

1. Introduction

Until 2012, the local interstellar magnetic field (IsMF) could only be determined indirectly. Lallement et al. (2005, 2010) analyzed Solar and Heliospheric Observatory (SOHO)/Solar Wind ANisotropy (SWAN) instrument data on backscattered Lyman-$\alpha$ emission and concluded that the direction of the interstellar neutral hydrogen flow in the heliosphere is deflected by $\sim 4^\circ$ from the direction of the pristine (i.e., undisturbed by the interaction with the Sun) local interstellar gas flow. The deflection is due to distortion of the global shape of the heliosphere under the action of the inclined interstellar magnetic field. The interstellar H atoms pass through the heliospheric interface and interact with the plasma component by charge exchange. Imprints of the asymmetry of the heliospheric plasma interface in the distribution of the interstellar H atom component appear as an observed deflection of the H atom flow as compared with the interstellar helium. Lallement et al. (2005) suggested that the plane determined by the velocity vectors of interstellar helium and hydrogen inside the heliosphere coincides with the plane determined by the vectors of velocity, $V_{\text{LISM}}$, and magnetic field, $B_{\text{LISM}}$, of the pristine local interstellar medium. This plane is often referred to as the (BV)-plane or hydrogen deflection plane (HDP). Izmodenov et al. (2005a, 2009) applied their 3D kinetic-magnetohydrodynamical (MHD) models of the solar wind (SW) interaction with the local interstellar medium (LISM) and confirmed the value of deflection angle observed by Lallement et al. (2005). Later, Katushkina et al. (2015) studied the deflections in detail and confirmed these previous conclusions.

The second way to put constraints on the LISM magnetic field is the asymmetry of heliospheric termination shock (TS) in Voyager 1 and 2 directions. Indeed, Voyager 1 crossed the TS at 94 AU in 2004 while Voyager 2 at 84 AU in 2007. It was surprising that Voyager 2 crossed the TS closer by 10 AU because the trajectory of Voyager 2 was further away from the direction of interstellar flow as compared to Voyager 1. Therefore, prior to the crossing it was expected that the TS distance in Voyager 2 direction was larger than 94 AU. However, the solar wind dynamic pressure decreases in the period from 2004 to 2007, and so in this time period the TS moved toward the Sun (e.g., Izmodenov et al. 2008). Nevertheless, these time variations can explain only a small part of the TS asymmetry. The main reason for the asymmetry of the global heliosphere, and in particular the termination shock, is the inclined interstellar magnetic field. The strength of the magnetic field should be large enough to create the asymmetry. Izmodenov & Alexashov (2015) employed the latest version of a 3D kinetic-MHD model of the global heliosphere and concluded that the model with an interstellar magnetic field of $B_{\text{LISM}} \approx 4.4 \mu G$ in magnitude and $(163.5^\circ, 18^\circ)$ in direction (in heliographic inertial (HGI) coordinate system) provided termination shock distances in Voyager 1 and 2 directions that are comparable with the distances of actual crossings. However, the distance to the heliopause obtained in the frame of this model was $\sim 164$ AU, which is very far from the actual distance of the heliopause crossing by Voyager 1 of 122 AU. It was suggested that this discrepancy can be explained by a dissipation mechanism in the inner heliosheath (e.g., Izmodenov et al. 2014; see also discussions in Izmodenov & Alexashov 2015; Izmodenov 2018).

Another way to determine the magnitude and direction of the pristine interstellar field is to analyze the ribbon of enhanced fluxes of heliospheric energetic neutral atoms (ENAs) that was discovered by Interstellar Boundary Explorer (IBEX;
2. Preliminary qualitative consideration

The magnetometers onboard Voyager 1 and 2 measured, for the first time, the interstellar magnetic field after they crossed the heliopause. A detailed comparison of the magnetic field components measured by Voyagers 1 and 2 with those obtained in the model are provided in the following section. In this section we consider the consequences of two observational phenomena: (1) the radial component of the magnetic field $B_R$ is positive in Voyager 1 direction, and negative but close to zero in Voyager 2 direction; and (2) the $B_T$ component of the magnetic field in radial tangential normal (RTN) coordinate system (see, e.g., Happgood 1992) is negative in both directions. These facts provide restrictions on the local shape of the heliopause in directions of crossings and also on the topology of the interstellar magnetic field around the heliopause (Burlaga et al. 2018, 2019a,b; see also Fig. 3).

If we assume an ideal nondissipative approach (as in the model) then the heliopause is a tangential discontinuity at which $B_n = 0$, where $B_n$ is the projection of the magnetic field vector to the normal of the heliopause surface. Therefore, the magnetic field vector should be parallel to the surface of the heliopause. In this case, the sign of the $B_R$ component depends on the local shape of the heliopause. If the heliopause is locally spherical then $B_R = 0$. If the projection of the normal $n$ to the heliopause on the X-axis (towards the heliopause) is larger than the X-axis projection of the unit radius vector then a heliopause has a blunt shape (Fig. 1, panel A1). Otherwise, the shape is oblong (Fig. 1, panel A2). The sketches in panels A1 and A2 also show that in the case of negative $B_T$: $B_R > 0$ for the blunt shape, and $B_R < 0$ for the oblong case. If the direction of the magnetic field is opposite (not shown in the sketches), then $B_R < 0$ for the blunt shape, and $B_R > 0$ for the oblong case. In the direction of Voyager 1, $B_T < 0$ and $B_R > 0$, and therefore the heliopause has to have a blunt shape in this direction. In the direction of Voyager 2, $B_T < 0$ and $B_R < 0$, and therefore the heliopause has to have an oblong shape in this direction.

The fact that $B_T$ is negative in both Voyager 1 and Voyager 2 directions also means that the critical point of the magnetic field (i.e., the point of $B = 0$) at the heliopause should be either above Voyager 1 or below Voyager 2 directions. The two possible cases with $B_T < 0$ are shown in panels B1 and B2 of Fig. 1 (see, also, panels C1, C2 for another projection). In the case of panel B1(C1) the critical point is above Voyager 1, and in the case of panel B2(C2), the critical point is below Voyager 2. If the critical point is located between Voyager 1 and Voyager 2 directions then the sign of $B_T$ will be different in these directions. This is illustrated in panels B3 and C3 of Fig. 1. Panels B1–C3 present the results of model calculations; these are shown for illustrative purposes only.

In the vicinity of the magnetic field critical point, the magnetic tension stretches the heliopause out of the Sun (see, Baranov & Zaitsev 1995). This causes the shape of the heliopause to be locally blunt in a significant part of it close to the stagnation point. At the same time, in the other hemisphere, where the magnetic field is almost tangential, the magnetic pressure pushes the heliopause closer to the Sun.

Panels B1 and B2 of Fig. 1 clearly illustrate the stretching and pushing of the heliopause. In the case of panel B1 the heliopause has a blunt shape in Voyager 1 direction and an oblong shape in Voyager 2 direction. Therefore, $B_R > 0$ and $B_R < 0$ in Voyager 1 and 2 directions, respectively. These calculations are in the agreement with the observations of Voyager. For the case shown in panel B2, the heliopause is oblong and $B_R < 0$ in Voyager 1 direction, while the heliopause is blunt and $B_R > 0$ in Voyager 2 direction. Therefore, the case of panel B2 should be ruled out.

We conclude in this section that the signs of $B_R$ and $B_T$ components measured in Voyager 1 and 2 directions provide
qualitative constraints on the magnetic field configurations in the vicinity of the heliopause. Namely, the configuration should be qualitatively similar to the case shown in panel B1, that is, the critical point of the magnetic field should be above the Voyager 1 direction. The scenarios shown in panels B2 and B3 are ruled out.

3. Results and comparison with Voyager data

In this section, we present the results of the model with \( B_{LIS} = 3.75 \mu G \) and \( \alpha = 60^\circ \) (referred to as Model 1), where the magnetic field belongs to the hydrogen deflection plane and \( \alpha \) is the angle between vectors of the interstellar velocity and magnetic field. The direction of the interstellar magnetic field in the HGI system is \( \approx 125^\circ \) in longitude and \( \approx 37^\circ \) in latitude. For comparison, the results of the model from Izmodenov & Alexashov (2015) with \( B_{LIS} = 4.4 \mu G \) and \( \alpha = 20^\circ \) are also shown and are referred to as Model 2. We note that both models are “Voyager permitted” that is, they correspond qualitatively to the case shown in panel B1 in Fig. 1.

Before comparing the model results with data obtained by the Voyager spacecraft, we present (Fig. 2) fluctuations of the heliospheric termination shock and the heliopause with time. The termination shock fluctuates by \( \sim 12_{-15}^{+15} \) AU from minimal to maximal distance depending on the direction that is in agreement with previous time-dependent models (Izmodenov et al. 2005b, 2008). The heliopause distances obtained by Model 1 are \( \sim 123.5 \) AU in August 2012 for Voyager 1 direction and \( \sim 121.5 \) AU in November 2018 for Voyager 2 direction. These distances do not exactly coincide with the distances of actual heliopause crossings by Voyagers, but are closer than the results obtained in the frame of Model 2, which are \( \sim 170 \) AU and \( 141 \) AU, respectively. Such a dramatic difference in the distances to the heliopause and in the heliopause asymmetry demonstrates that the angle \( \alpha \) between \( \mathbf{V}_{LIS} \) and \( \mathbf{B}_{LIS} \) vectors is very important. The larger the angle, the closer the perpendicular component of the magnetic field pressure pushes the heliopause toward the Sun, and the smaller the parallel component that makes the heliopause more asymmetric (for \( \alpha \neq 0 \)). The model results show that the heliopause moves inside from 2009 to 2016 and then moves outside. This is surely connected with the minimum of the solar wind dynamic pressure from 2007–2008 to 2015 as seen in Fig. A.1. It is interesting to note that although the excursions of the TS with time are quite similar in the two presented models, the small-scale details are different. We connect this with the difference in the global shape of the heliopause.

The distances to the termination shock are \( \sim 84 \) AU in September 2004, and \( \sim 78 \) AU in July–August 2007. Therefore, Model 1 does not reproduce a 10 AU difference from the actual distances of Voyager 1 and 2 crossings, but reproduces a \( \sim 6 \) AU difference, which is a significant fraction of 10 AU. The model distances to the TS are by 10 AU and 6 AU (for Voyager 1 and 2, respectively) smaller as compared with actual Voyager crossings.

Now let us compare the magnetic field component obtained in Model 1 with the actual Voyager data. The comparison of the model results with Voyager data in the inner heliosheath is not a major aim of this study, but is discussed in Appendix B. Here we focus on the comparison of the magnetic field components in the outer heliosheath beyond the heliopause.

Figure 3 presents the magnetic field and plasma velocity components along the Voyager 1 and 2 trajectories in the RTN coordinate system as a function of time. Voyager data are shown as solid curves. Voyager 1 Magnetometer (MAG) data plotted in Fig. 3A were obtained from the NASA website. These data were presented and discussed in Burlaga et al. (2018, 2019a). Voyager 2/MAG data were obtained from Fig. 3 of Burlaga et al. (2019b). Model results are shown as dashed curves. Since the distances to the heliopause obtained in the model are larger than those measured from observations, we shifted the model distances by \( \Delta R = R_{model} - R_{data} \) closer to the Sun and did not make any time shift. Here, \( \Delta R \) is 3 AU in Voyager 1 direction and 5 AU in Voyager 2.

The model–data comparison shows that just beyond the heliopause all three components of the interstellar magnetic field of Model 1 match those measured by both Voyagers (Figs. 3A and B). Data for Voyager 2 are restricted by the closest vicinity of the crossing, while Voyager 1 magnetometer data after the heliopause crossing are publicly available from 2012 until the end of 2017. Therefore, we can compare how the three components of the magnetic field behave along the Voyager 1 trajectory. Figure 3A shows that the \( B_{R} \) and \( B_{T} \) components match the data for the entire period of available observations. However, the small-scale details of the component fluctuations are different between the model and data; the model results are smooth. We associate these differences with the inner boundary conditions taken at 1 AU which are 27-day averages.

The most significant difference between Model 1 and the data exists for the \( B_{R} \) component. In the Model, \( B_{R} \) remains almost constant for the entire period from 2012 to 2017 and beyond, while in the data, the \( B_{R} \) component is almost constant for 2013–2014 and then gradually decreases. Two bumps on the generally decreasing slope are associated with disturbances induced by merged interaction regions (Burlaga et al. 2018, 2019a). Possible reasons for and implications of the difference in the \( B_{R} \) component are discussed in the following section.

4. Conclusions and discussion

We have found a combination of magnitude and direction of the interstellar magnetic field \( B_{LIS} = 3.75 \mu G, \alpha = 60^\circ \) for which the model reproduces the positions of the heliopause in Voyager

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1. [https://cohoweb.gsfc.nasa.gov](https://cohoweb.gsfc.nasa.gov)
Fig. 3. Components of the magnetic field (panels A and B) in the RTN coordinate system along the Voyager 1 (panel A) and Voyager 2 (panel B) trajectories. The results of Model 1 are shown as dashed curves. Solid curves represent Voyager 1/MAG data in panel A and Voyager 2/MAG data in panel B. The model curves are shifted by 3 AU in panel A, and by 5 AU in panel B.

1 and 2 directions reasonably well at the times of actual crossings. The difference of 2.5 AU is insignificant and can easily be removed by a slight increase of proton or H atom number densities. At the same time, the distance to the termination shock obtained in the model is 84 AU in 2004 in Voyager 1 direction. This is 10 AU closer than the actual distance. However, the model shows that in 2004–2005 the distance of the termination shock fluctuates rather strongly; this is connected with variations of the solar wind parameters. In reality, the variations are expected to be much stronger than in the model. Indeed, the angular resolution is 10 degrees in latitude and the time-resolution is 27 days in the model. Stronger time variations of the termination shock can in principle reduce the model–data difference in the termination shock distance. In Voyager 2 direction, the TS is 5.5 AU closer to the Sun in the model as compared to the actual crossing.

Therefore, the thickness of the inner heliosheath is ~8 AU larger in the model. This difference is much smaller than for the model reported in Izmodenov & Alexashov (2015; referred to here as Model 2). Nevertheless, the difference is significant. We suppose that it may be due to some yet unknown dissipation process in the inner heliosheath. The possible candidates were discussed in previous papers by Izmodenov et al. (2014) and Izmodenov & Alexashov (2015).

The model reproduces all three magnetic field components just after the heliopause crossings by Voyager 1 and Voyager 2. The comparison of the model and data along the trajectory of Voyager 1 shows that $B_R$ and $B_N$ components are predicted by the model relatively well. Radial component $B_R$ decreases in 2016–2017 in the data and remains constant in the model.

It is important to note that the interstellar flow in the model is subsonic with respect to fast magnetosonic waves (i.e., fast magnetosonic Mach number is smaller than one). Therefore, there is no bow shock and, theoretically, interstellar flow is perturbed by the interaction with the Sun up to very large distances. However, from the numerical results (see Figs. 1 and B.1) it is seen that at distances of ~500 AU in the upward direction the magnetic field lines are aligned only very weakly and the interstellar parameters are close to those in the pristine LISM.

As discussed in Appendix B, in the inner heliosheath, the model reproduces $V_R$ and $V_T$ components in Voyager 1 direction relatively well (B.1). In the direction of Voyager 2, the model reproduces $V_R$ and $V_T$ components just after the termination shock. However, at larger distances, the components obtained in the model behave differently as compared to Voyager 2 plasma data. Apparently, the model reproduces the flow in Voyager 1 direction and does not reproduce it in Voyager 2 direction. As for the heliospheric magnetic field, the model shows a significant increase towards the heliopause that is not observed. The deficit of the magnetic field is probably due to a dissipation process. The magnetic field dissipation could also be the reason for the difference in the inner heliosheath plasma flow.

In the qualitative discussion of Sect. 2, we implicitly assumed that the shape of the heliopause is determined by the interstellar magnetic field. However, it has been shown (Izmodenov & Alexashov 2015) that heliolatitudinal dependence of the solar wind dynamic pressure and heliospheric magnetic field influence the shape of the heliopause. In addition, but to a lesser extent, time variations may temporarily affect the heliopause shape locally. All these effects are taken into account in our model, and they are essential for the model results matching the data at the heliopause.

The model–data difference in $B_R$ along the Voyager 1 trajectory may be connected with the time fluctuations. Indeed, when the heliopause moves in and out it acts as a piston; moving in, it compresses the magnetic field lines. Therefore, the tangential components of the interstellar magnetic field increase. The radial motion of the heliopause should increase the $B_R$ component as well because the direction of the magnetic field should be parallel to the heliopause surface. The fact that fluctuations of all magnetic field components correlate is clearly seen in both Voyager 1 data and in the model results (Fig. 3A). However, the level of fluctuations in the model is somewhat smaller than in the data. This may be connected with the dataset for the solar wind parameters that we employed in the model. For example, it may be due to the 27-day time averaging that was performed for the solar wind parameters in the model. Averaging indeed reduces the level of fluctuation. In addition, some instabilities may occur at the heliopause which are not considered in the model.

We also compared the results of the presented model with other constraints of the SW/LISM interaction model: (1) The magnetic field chosen for Model 1 belongs to the hydrogen deflection plane established by Lallement et al. (2010); the angle
between the direction of the interstellar hydrogen and helium in the outer heliosphere (for instance at 60–70 AU) is ≈3.5° which is similar to the deflection obtained by Lallement et al. (2010). (2) The interstellar hydrogen number density in the outer heliosphere is ≈0.1 cm⁻³ which is similar to the number density established previously by different methods, e.g. by analyses of the supersonic solar wind deceleration (Wang & Richardson 2003), by analyses of Ulysses pickup protons data (Gloeckler et al. 1997), by analyses of SOHO/SWAN backscattered solar Lyman alpha data (Quémerais et al. 2013). (3) The direction of the magnetic field of Model 1 (≈125°, ≈37°) in HGI is not too far from the direction derived by Zirnstein et al. (2016) from analyses of IBEX ribbon (147.5°, 31°), although some difference exists in both direction and magnitude. We plan to analyze the IBEX ribbon using our model in the future.

It is important to note that our numerical calculations were not restricted to only Models 1 and 2. We performed very intensive (although not completely systematic) parametric calculations by varying the magnitude of the interstellar magnetic field, the angle α, and the interstellar proton and H atom number densities. Since our model requires us to solve 3D time-dependent MHD equations self-consistently with a 6D kinetic equation, such parametric calculations are extremely computationally expensive. This explains why we do not match the locations of the heliopause in Voyager 1 and Voyager 2 exactly. Such an “exact” result would be computationally expensive but of little use because of averaging of the solar wind parameters at the inner boundary. Nevertheless, Model 1 presented in this Letter is the best model of many (about 50) considered models. Figure 4 presents (as an example) results of calculations with nine different model parameters. Model 1 is shown in panel A as a reference. The models with a larger interstellar field (one is shown in panel B) were ruled out because they produce a larger magnetic field at the heliopause as compared with Voyagers as well as smaller distances to the heliopause and especially to the termination shock. The models with reduced magnitude of the magnetic field (panels D, E, F) produce a smaller magnetic field at the heliopause in Voyager 2 direction and opposite (as compared with Voyagers) asymmetry of the heliopause in Voyager 1 and 2 directions. Attempts to reduce the angle α (panel C) lead to a strong increase of the heliocentric distances to the heliopause. In fact, it is also possible to produce the exact magnitude of the magnetic field at the heliopause in the models with a rather small magnetic field in the pristine LISM. To do that, we had to increase the dynamic pressure of the plasma component by increasing the interstellar proton number density (panels G, H, I). However, in this case, the heliopause became quite axis-symmetric and heliocentric distance to the heliopause became significantly larger in Voyager 2 direction as compared with Voyager 1. Therefore, such models were ruled out as well.

Here, we demonstrate qualitatively that the information on the interstellar magnetic field in Voyager 1 and 2 directions provides us with strong constraints on the direction and magnitude of the pristine interstellar magnetic field. Numerical results demonstrate that Model 1 matches the data relatively well but not completely. Further numerical studies will perhaps allow a model to be found that will fit the data better, but the resulting magnitude and direction of the interstellar magnetic field should not be too different from those presented here.

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Fig. 4. Global shape of the heliopause, interstellar magnetic field lines, and magnitude in the outer heliosheath obtained for different model parameters.
Appendix A: Model and boundary conditions

In this appendix we give a brief summary of the basic features of the Izmodenov & Alexashov (2015) model and discuss the boundary conditions used in time-dependent calculations presented here. The detailed formulation of the physical and numerical model is given in Izmodenov & Alexashov (2015). In the model, partially ionized interstellar plasma is considered as a two-component gas. The two components are (1) a neutral component consisting of atomic hydrogen and (2) a charged (or plasma) component consisting of protons, electrons, and helium ions. In the solar wind, the plasma component consists of protons, alpha particles, and electrons. The neutral component is described kinetically. The charged (plasma) component is described in the context of an ideal MHD approach.

The influence of charge exchange with the interstellar H atoms was taken into account in the right-hand side of the MHD equations by the source terms. Source terms have been calculated using the Monte Carlo method (Malama et al. 2001). This method assumes that the velocity distribution function of the plasma component is locally Maxwellian, although it allows a generalization to any isotropic distribution function as was done by Malama et al. (2006).

The inner boundary for our model is located at 1 AU. We take into account helio-latitudinal variations of the SW density and speed at 1 AU obtained by using three different sets of data:

1. In the ecliptic plane, we use data (SW density and speed) from the OMNI 2 dataset\(^2\). The OMNI 2 data set contains hourly resolution SW magnetic field and plasma data from many spacecraft in geocentric orbit and at the L1 Lagrange point.

2. Heliolatitudinal variations of the SW speed are taken from analysis of the interplanetary scintillation (IPS) data (Tokumaru et al. 2012\(^3\)). Data are available from 1990 to 2017.

3. Heliolatitudinal variations of the SW mass flux are derived from analysis of SOHO/SWAN full-sky maps of the backscattered Lyman-alpha intensities (Quémerais et al. 2006; Lallement et al. 2010; Katushkina et al. 2013, 2019).

An inversion procedure (see Quémerais et al. 2006 for details) allows us to obtain the SW mass flux as a function of time and heliolatitude with a temporal resolution of approximately 1 day and an angular resolution of \(10^\circ\). Data are available from 1995 to the end of 2017.

From these data, we calculate the mass and momentum fluxes of the SW as functions of time (from 1995 to 2017) and heliolatitude. We note that a similar procedure was followed to obtain the boundary conditions in Izmodenov & Alexashov (2015) with further averaging of the parameters over the entire time period. The distribution of the solar wind proton number density and velocity at 1 AU as functions of time and heliolatitude are shown in Fig. A.1. The solar wind dynamic pressure is shown in Fig. A.1 (plot C) as well. The heliospheric magnetic field is described exactly as it was in Izmodenov & Alexashov (2015), so we do not repeat it here.

The interstellar bulk velocity and temperature are chosen as \(V_{\text{LISM}} = 26.4 \text{ km s}^{-1}\) and \(T_{\text{LISM}} = 6530 \text{ K}\). This velocity value is consistent with the ISM vector derived from analyses of Ulysses/GAS data for interstellar helium (Witte 2004; Bzowski et al. 2014; Katushkina et al. 2014; Wood et al. 2015). The direction \(V_{\text{LISM}}\) is determined by the interstellar helium flow direction from Ulysses/GAS data. This value is (longitude = \(-1.02^\circ\), latitude = \(-5.11^\circ\)) in the heliographic inertial coordinate system (HGI 2000). The velocity vector is in agreement with new results derived from IBEX data (see, e.g. McComas et al. 2015).

The interstellar H atom and proton number densities are assumed to be the same as in Izmodenov & Alexashov (2015): \(n_{\text{H,LISM}} = 0.14 \text{ cm}^{-3}\) and \(n_{\text{p,LISM}} = 0.04 \text{ cm}^{-3}\), respectively. The number density of the interstellar helium ions that provide additional pressure (see Izmodenov et al.; Izmodenov & Alexashov 2015) is chosen as \(n_{\text{He+,LISM}} = 0.003 \text{ cm}^{-3}\).

The remaining parameter is the IsMF. As in Izmodenov & Alexashov (2015) we assume that the plane which is determined by the vectors \(V_{\text{LISM}}\) and \(B_{\text{LISM}}\) coincides with the plane determined by the velocity vectors of the interstellar helium, \(V_{\text{He}}\), and hydrogen, \(V_{\text{H}}\), inside the heliosphere – the so-called hydrogen deflection plane (HDP; see, Lallement et al. 2005, 2010; for model justification see Izmodenov et al. 2005b, 2009). Under this assumption, the

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\(^2\) https://omniweb.gsfc.nasa.gov/
\(^3\) http://stswl.isee.nagoya-u.ac.jp/annual_map.html
IsMF is determined by its magnitude and by the angle with the direction of the interstellar bulk flow, \( V_{H, \text{LISM}} \). This angle is denoted as \( \alpha \). Izmodenov & Alexashov (2015) assumed \( B_{\text{LISM}} = 4.4 \mu \text{G} \) and \( \alpha = 20^\circ \). The values were obtained in the parametric study presented in Table 2 of Izmodenov et al. (2009) to obtain asymmetry of the TS in agreement with the distances of the Voyager 1 and Voyager 2 TS crossings. However, as was shown by Izmodenov & Alexashov (2015), our model with such an IsMF obtains the heliopause at very large distances, which are in disagreement with the actual Voyager crossings of the heliopause.

**Appendix B: Comparison of the model with Voyager data in the inner heliosheath**

Although comparison of the model results with Voyager data from the inner heliosheath (i.e., the region between the termination shock and the heliopause) is not the major purpose of this Letter, it is presented in Fig. B.1 as well. Figure B.1 (panel C) shows \( V_R \) and \( V_T \) plasma velocity components obtained in Model 1 with those derived from analyses of anisotropy of energetic particle fluxes (Krimigis et al. 2011). Relatively good qualitative agreement of model and data was obtained. The \( V_R \) component is about \( \sim 100 \text{ km s}^{-1} \) after the decreases and becomes zero or sometimes negative as the spacecraft approaches the stagnation region (Krimigis et al. 2011). The \( V_T \) component is about \( 30–40 \text{ km s}^{-1} \) at the TS and slowly decreases toward the stagnation region.

Comparison of the model results with Voyager 2/PLS data is shown in Fig. B.1 (panel D). Up to now these data were only available for the period up to October 1, 2018, that is before Voyager 2 crossed the heliopause. First of all, although not shown in the figure, we notice that the model reproduces the speed and its fluctuations in the supersonic solar wind reasonably well. The location of the TS is closer in the model by \( \sim 5 \text{ AU} \) in Voyager 2 direction. Just after the TS, the magnitudes of the \( V_R \) and \( V_T \) components of velocity coincide with the data remarkably well. As the spacecraft moves out, the \( V_R \) component decreases both in the model and in the data. However, the decrease obtained in the model is much faster. The \( V_R \) component behaves in Voyager 2 direction in the similar way as it was observed earlier in the direction of Voyager 1. This is not observed in Voyager 2/PLS data. The \( V_T \) component remains almost constant (or slowly decreases) in the model, while in the data this component increases from \( \sim 80 \text{ km s}^{-1} \) just after the TS crossing to \( \sim 100 \text{ km s}^{-1} \). The \( V_N \) component is larger in the model immediately after the shock. It is interesting enough that for the distances larger than 90 AU the model reproduces V2 observations for this component relatively well.

Finally, we compare the magnetic field in the inner heliosheath (Fig. B.1, panels A and B). The magnetic field (mostly \( B_T \) component) obtained in the model can be seen to significantly increase towards the heliopause. This is the magnetic pile-up region that was discussed in Izmodenov & Alexashov (2015) in detail. It is important to note that this effect is obtained in the frame of an ideal MHD approach. The fact that it is not observed may suggest that there is effective dissipation of the magnetic field in this region.

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**Fig. B.1.** Components of the magnetic field (panels A and B) and plasma velocity (panels C and D) in RTN coordinate system along the Voyager 1 (top panels) and Voyager 2 (bottom panels) trajectories in the inner heliosheath. Results of Model 1 are shown as dashed curves. Solid curves represent Voyager 1/MAG data in panel A. Voyager 2/MAG data in panel B. \( V_N \) and \( V_T \) derived by Krimigis et al. (2011) from analyses of energetic particle anisotropy measured by Voyager 1/LECP are shown as dots in panel C. Dots in panel D show Voyager 2/PLS data.