Variability of the Initial Abstraction Ratio in an Urban and an Agroforested Catchment

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Abstract: The Curve Number method is one of the most commonly applied methods to describe the relationship between the direct runoff and storm rainfall depth. Due to its popularity and simplicity, it has been studied extensively. Less attention has been given to the dimensionless initial abstraction ratio, which is crucial for an accurate direct runoff estimation with the Curve Number. This ratio is most often assumed to be equal to 0.20, which was originally proposed by the method’s developers. In this work, storm events recorded in the years 2009–2017 in two small Polish catchments of different land use types (urban and agroforested) were analyzed for variability in the initial abstraction ratio across events, seasons, and land use type. Our results showed that: (i) estimated initial abstraction ratios varied between storm events and seasons, and were most often lower than the original value of 0.20; (ii) for large events, the initial abstraction ratio in the catchment approaches a constant value after the rainfall depth exceeds a certain threshold value. Thus, when using the Soil Conservation Service-Curve Number (SCS-CN) method, the initial abstraction ratio should be locally verified, and the conditions for the application of the suggested value of 0.20 should be established.

Keywords: Curve Number; initial abstraction ratio; direct runoff; SCS-CN method; small catchment

1. Introduction

Estimation of the direct runoff as a catchment response to a rainfall or snowmelt event is important for many practical applications: The direct runoff is the key variable used for designing hydraulic structures [1], estimating soil erosion and sediment yield [2], or analyzing long-term changes in water resources availability [3]. The amount of water outflowing after a storm event depends on, among others, the catchment topography, land cover, soil characteristics, and climate conditions. Hence, for a specific site, the amount of direct runoff may vary significantly over successive years but also from one storm event to another within the same year [4]. This relationship between the direct runoff and the storm rainfall depth may be assumed constant given the same rainfall depth and unchanged catchment conditions.

One of the most commonly applied methods to describe this relationship between the direct runoff and storm rainfall depth is the Soil Conservation Service-Curve Number (SCS-CN), developed by the United States Department of Agriculture (USDA) [5]. Despite its simplicity, this method accounts for most of the catchment runoff characteristics responsible for producing the direct runoff such as soil type; land use and treatment; and surface and antecedent moisture conditions. Moreover,
its parameter (i.e., curve number, CN) can be derived directly from physical properties of the catchment or from recorded rainfall-runoff events [6]. Therefore, the SCS-CN method remains very attractive for runoff estimation in poorly gauged regions, in applied hydrology for engineering designs, or in post analysis of recorded data [7,8], where the simplicity and the universality of the method play a deciding role. As this method estimates only the direct runoff without considering the base flow component, it is most often applied to event-based models [9]. According to SCS-CN, the relationship between the rainfall depth, direct runoff, and catchment retention can be described as follows:

\[
\frac{H}{P - Ia} = \frac{F}{S}
\]  

(1)

where:
- \(F\): actual catchment retention (mm),
- \(S\): potential maximum catchment retention (mm),
- \(H\): direct runoff, effective rainfall (mm),
- \(P\): rainfall depth (mm),
- \(Ia\): initial abstraction (mm).

Note that, \(F \leq S\) and \(H \leq (P - Ia)\). The total retention for a storm consists of both \(Ia\) and \(F\), so the conservation of the mass Equation can be expressed as:

\[
F = P - Ia - H
\]  

(2)

Substituting Equation (2) for \(F\) in Equation (1) and solving it for the direct runoff results in:

\[
H = \frac{(P - Ia)^2}{P - Ia + S}
\]  

(3)

The initial abstraction \((Ia)\) consists of evaporation, interception, infiltration, and surface depression storage. If rainfall depth is lower or equal to the initial abstraction, the direct runoff is assumed to be zero (i.e., all rainfall water is used to fill the catchment retention). According to the National Engineering Handbook [5], an empirical relationship between \(Ia\) and \(S\) has been established as:

\[
Ia = \lambda \times S
\]  

(4)

where \(\lambda\) is the initial abstraction ratio (-).

The potential maximum catchment retention \((S)\) is next calculated from the following formula:

\[
S = 25.4 \left(\frac{1000}{CN} - 10\right)
\]  

(5)

where \(CN\) is curve number, i.e., the only parameter (-) of the SCS-CN method that depends on soil characteristics, land use, and catchment initial conditions prior to the storm event.

Due to its popularity, the SCS-CN method has been the object of many studies. These studies focused on application of the method, e.g., in rainfall-runoff modelling [10], analyzing the impact of land use changes such as urbanization on runoff values [11], predicting sediment yield [12,13], as well as on the estimation and verification of the \(CN\) parameter [14–17]. Yet, less attention has been given to the dimensionless initial abstraction ratio \((\lambda)\), and most often this ratio was assumed equal to 0.20, as it was originally proposed by method’s developers [5]. Although Woodward et al. [18] have suggested based on intensive data of 327 US catchments that a value of 0.05 may be more appropriate than 0.2, most of the applied studies continued to use the originally proposed value of 0.2. Recently, this dimensionless initial abstraction ratio \((\lambda)\) has gained much more attention and several researchers have revealed that a) this ratio may vary widely for specific sites [19,20], and b) it may be significantly lower than 0.2 [18,21,22]. A change in the initial abstraction ratio from a fixed value of 0.20 to a lower value will strongly affect the estimated depth of the direct runoff and consequently the direct runoff distribution over time. Durán-Barroso et al. [23] have even stated this relationship between the initial abstraction and the maximum potential catchment retention as being
one of the major sources of uncertainty in the SCS-CN method. Hence, some researchers have tried to estimate the value of this ratio from recorded storm data, and they concluded that using a varying value of the initial abstraction ratio rather than a fixed value of 0.2 or even 0.05 significantly improves runoff estimates [9,20,23]. Nevertheless, the number of studies devoted to the initial abstraction ratio is still very limited. As this ratio was also declared as being regional specific [18], more research is needed for catchments in different climatic regions to investigate properties of this ratio.

Another important aspect of the initial abstraction ratio is linked with the basic assumption of the SCS-CN method that both this ratio and the CN parameter are assumed constant given that catchment conditions do not change. Yet, any change in the catchment conditions will affect the relationship between the storm rainfall depth and the direct runoff amount, and consequently the value of the CN parameter and possibly the initial abstraction ratio. In this respect, direct human activities such as land use changes and human induced climate changes are considered as two major factors that affect runoff processes the most. Many studies have tried to quantify their role in the hydrological cycle [24–26]. For instance, Chen et al. [27] revealed that for a large basin (area = 18,827 km²) in northwestern China, climate variability was the major factor affecting the runoff amount, accounting for 90.5% of the increase in the runoff amount, while other human activities accounted only for 9.5% of the runoff increase. In contrast to that, Lv et al. [28] found for the same region that in the case of a small catchment (area = 72.8 km²), climate change accounted only for about 33% of the total decrease in mean annual runoff, while direct human activity was responsible for about 67% of the decrease in mean annual runoff. Tan and Gan [29], based on investigations in 96 Canadian catchments, showed that climate change generally caused an increase in the mean annual runoff, while direct human impacts usually lead to decreasing water resources. These studies indicate how complex interactions between climatic, anthropogenic, and hydrological variables are, and how difficult it is to evaluate their individual impacts on the hydrological cycle in the catchment [30]. Although these climatic and direct anthropogenic factors can be accounted for in the SCS-CN method by simply adjusting the curve number (CN), it remains unclear whether and how exactly these factors may affect the value of the initial abstraction ratio in the SCS-CN method.

In this work, recorded rainfall-runoff data collected in the years 2009–2017 in two small Polish catchments of different land use types (urban and agroforested) were analyzed in order to a) estimate and verify the value of the initial abstraction ratio in these two catchments for different storm events, b) analyze the variation of the initial abstraction ratio with the rainfall depth, and c) explore (indirectly) the effect of the land use type and season on the initial abstraction ratio value in this climatic region. The main focus of this study is to investigate such local estimates of the initial abstraction ratio based on limited recorded storm events for two small catchments of different land use types. This study is a follow-up of two previous studies conducted for these two catchments [14,31] that investigated the applicability of the SCS-CN method and estimated the CN parameter values based on conventional methods. Therefore, the estimation of the CN and its verification are not the main subjects of this study.

2. Materials and Methods

2.1. Characteristics of the Study Catchments

Data analyzed in this work were collected in two small catchments of different land use types: urban at Służew Creek and agroforested at Zagozdźonka River (Figure 1). In both of them, meteorological and hydrological variables are automatically monitored by the Department of Water Engineering and Applied Geology (DoWEaAG) of Warsaw University of Life Sciences-SGGW (WULS-SGGW). Table 1 presents basic topographic and climatic characteristics of both study sites. Both of these catchments are under human pressure. In the urban catchment of Służew Creek, for the last 40 years an increase of impervious areas has been observed, which, among others, leads to a higher flood risk [32]. In the agroforested catchment of Zagozdźonka River, decreasing trends in low and medium discharges have been observed [3]. Research on the rainfall-runoff process under the
above mentioned conditions is particularly valuable as it helps to manage water resources in a changing environment.

The first catchment, Służew Creek, is located in the southwestern part of Warsaw in Poland. Its total area equals 54.8 km², whereas the subcatchment up to Wyścigi gauging station (analyzed in this work) has an area of 28.7 km². This catchment has heterogeneous land use (see Table 2 for details) with more than 60% of its area covered by built-up areas and with the impervious factor of the total catchment reaching up to 25%. Fine-grained soils dominate the watershed area. Previous investigations conducted in the Służew Creek catchment were related to urban hydrology with a focus on flood flow estimation [33,34] and operation of small detention ponds for flood and sediment load reduction [35,36] or sediment transport [37,38]. The climate in Poland is continental and in the case of the analyzed study site it may be described as moderate. Long-term measurements indicate that the average annual precipitation is 541.9 mm [39] and the average annual temperature is 8.6 °C [40]. The average annual discharge at Wyścigi gauging station in the analyzed period (2009–2017) was 0.182 m³ s⁻¹ [41].

![Figure 1](image)

**Figure 1.** Locality map of Służew Creek (A) and Zagoźdzonka River (B) catchments up to the Wyścigi and Czarna gauging stations, respectively.

**Table 1.** Topographic and climatic characteristic of investigated catchments.

| Category                  | Unit          | Służew Creek (Years) [Source] | Zagoźdzonka River (Years) [Source] |
|---------------------------|---------------|-------------------------------|-----------------------------------|
| Catchment type            | -             | lowland, urbanized            | lowland, agroforested             |
| Area up to gauging station| km²           | 28.7 [41]                     | 23.4 [41]                         |
| Average channel slope     | %             | 1.1 [41]                      | 3.0 [41]                          |
| Impervious surfaces       | %             | 25.3 [42]                     | 0.56 [42]                         |
| Average precipitation     | mm            | 541.9 (1960–2009) [39]        | 612.0 (1963–2015) [3]             |
| Average temperature       | °C            | 8.6 (1970–2009) [40]          | 8.1 (1951–2015) [3]               |
| Average discharge per sq. km | dm³ s⁻¹ km⁻² | 6.34 (2010–2017) [41]        | 3.89 (2010–2017) [41]             |

The second analyzed catchment, Zagoźdzonka River, is a left tributary of the Vistula River. Its catchment is located in central Poland, about 100 km south of Warsaw (Figure 1). Hydrological research in the upper part of the Zagoźdzonka River has been conducted by WULS-SGGW since the 1960s. It was initiated to determine the water needs of the chemical plant. Over time, the scope of
investigation has expanded [2,4,10,31], and currently there are two stream gauging stations, at Plachty Stare (since 1962) and Czarna (since 1991), at which measurements of basic meteorological and hydrological parameters are carried out continuously. In contrast to the urban catchment mentioned above, the Zagożdżonka River catchment can be defined as agricultural and forested. The catchment area at Czarna (considered in this study) is equal to 23.4 km². Forests (45%) and arable lands (43%) cover a significant part of the catchment area (see Table 2 for details). Sandy soils are the major soil type in this catchment, while in local depressions and river flood plains, peaty soils may be found.

The relief in both catchments is typical for lowlands in Poland with an insignificant elevation variation. Thus, the catchment elevation does not play any relevant role in the runoff generation in these two catchments.

Table 2. Land cover and soil types in the Służew Creek catchment up to Wyścigi gauging station and in the Zagożdżonka River catchment up to Czarna station.

| Category                          | Land Cover (%) and Soil Structure (%) in Służew Creek | Zagożdżonka River |
|-----------------------------------|------------------------------------------------------|-------------------|
| Residential areas                 | 28.9                                                 | 3.6               |
| Airport                           | 19.3                                                 | -                 |
| Arable lands                      | 12.9                                                 | 43.4              |
| Forests                           | 12.5                                                 | 45.1              |
| Industrial areas                  | 9.4                                                  | -                 |
| Recreation areas                   | 7.9                                                  | -                 |
| Roads and associated lands        | 7.1                                                  | -                 |
| Meadows                           | 2.0                                                  | 7.8               |

| Soil type [43]                    |                                                      |                   |
|-----------------------------------|------------------------------------------------------|-------------------|
| Loamy sand                        | 50.5                                                 | -                 |
| Light loamy sand                  | 40.2                                                 | -                 |
| Organic soil                      | 9.3                                                  | -                 |
| Silt loam                         | -                                                    | 67.8              |
| Silt                              | -                                                    | 27.3              |
| Sand                              | -                                                    | 4.9               |

2.2. Recorded Data

Hydrological field investigations were carried out in both catchments according to the standard methodology recommended by the Polish Institute of Meteorology and Water Management, National Research Institute [44,45]. Rainfall depths were measured with the use of tipping-bucket rain gauges at four locations in the Służew Creek catchment and two in the Zagożdżonka River catchment. Recorded rainfall depths were summed up in 10 min intervals and the average rainfall over the catchment was calculated according to the Thiessen polygons method. River gauging stations at catchments outlets were equipped with staff gages and automatic, pressure water stage loggers. At these river gauging stations, water stages data were collected every 10 min. In order to estimate and verify the automated measurements, readings of the gage staff were regularly performed at least once a week. Recorded water levels were next converted to discharge values with the help of the rating curve method [46]. The rating curves were established at both sites with numerous hydrometric measurements, i.e., cross section area and flow velocity, conducted at low, medium, and high stages. These curves were verified each year to reduce the uncertainty in the rating curve method [3].

2.3. Selection of Storm Rainfall-Runoff Events

From all rainfall events recorded in the years 2009–2017, we selected only those events that generated a direct runoff. All of these events were caused by rainfall events in the spring-summer
seasons. This criterion led to a selection of 53 storm events in the Sużew Creek, and 42 storm events in the Zagożdżonka River, respectively, with an average direct runoff of about 3 mm (2.9 mm in Zagożdżonka River). The average rainfall depth of selected events was equal to 22.8 mm in the Sużew Creek and to 25.8 mm in the Zagożdżonka River.

Antecedent moisture conditions (AMC) were estimated for all 95 events (see Table 3). Within these events, 85 were classified as AMC I, seven as AMC II, and three as AMC III. Therefore, it can be stated that the majority of recorded events occurred during dry conditions. This finding is surprising because the analyzed period 2009–2017 was not extremely dry or less rich in water compared to previous years [47]. Thus, it is likely that the thresholds used to determine moisture conditions may not correspond to the climate of central Poland and should be adapted for this region in a future study.

### Table 3. Antecedent moisture condition (AMC) for analyzed events according to the Soil Conservation Service-Curve Number method.

| Antecedent Moisture Condition | Total Number of Events with 5 Days of Rainfall for Dormant Period | Total Number of Events with 5 Days of Rainfall for Vegetation Period |
|------------------------------|---------------------------------------------------------------|---------------------------------------------------------------|
| AMC I                        | (12 events) < 13 mm                                          | (73 events) < 35 mm                                          |
| AMC II                       | 13 mm ≤ (3 events) ≤ 28 mm                                   | 35 mm ≤ (4 events) ≤ 53 mm                                   |
| AMC III                      | (1 event) > 28 mm                                            | (2 events) > 53 mm                                           |

### 2.4. Estimation of the Initial Abstraction Ratio from Recorded Data

The initial abstractions were estimated based on recorded storm events (see Figures 2 and 3) as the sum of the rainfall depth after which a direct runoff begins (seen as an increase in water stage and river discharge). The volume of the direct runoff was calculated based on the measured hydrograph, e.g., by indicating the event start point (increase in river discharge after the rainfall begins), the event end point (change in the slope of the hydrograph falling limb), and by removing the base flow from the total runoff. The base flow was estimated following the straight-line separation method that is described in detail by Wanielista et al. [48]. The computed volume of the direct runoff was next divided by the catchment area, giving the runoff depth for each storm event. As the rainfall depth, the direct runoff, and the initial abstraction are known (measured or estimated), Equation (3) may be solved for the maximum potential catchment retention: S. Finally, the initial abstraction ratio was computed from Equation (4) for each recorded storm event. This technique of *la* estimation has been used in previous studies such as Shi et al. [8] and Ling et al. [49].

The estimated values for the initial abstraction ratio were compared with the original value of 0.2 that was suggested in the original version of the SCS-CN method [5].
2.5. Variability of the Initial Abstraction Ratio

In order to investigate seasonal variation in the initial abstraction ratio due to the state of the vegetation development and other seasonal factors, the recorded storm events were next grouped into three periods: (I) beginning of the vegetation season (April–May), (II) full vegetation state (June–August), and (III) end of the vegetation season and plants resting period (September–March). The analysis of the initial abstraction ratio was performed for all events in each group separately and the estimated values for each group were compared.

Finally, we investigated whether a relationship between the initial abstraction ratio and the rainfall depth can be established for our recorded data. The relationship between the CN parameter and the rainfall depth has been explored [14,31,50]. Among others, Soulis and Valiantzas [51,52] studied the effect of soils and land cover variability on the hydrologic response and proposed a methodology to determine the spatial distribution of the SCS-CN parameter values from rainfall-runoff data. However, similar analyses of the initial abstraction ratio have rarely been performed [8,20] and did not reveal any relationships between these two variables. In our case, we focused only on summer events (i.e., from May to September), to reduce the possible effect of the seasonal variability in the ratio in the studied catchments and also because most of the recorded events occurred during this period.

The relationship between the initial abstraction ratio and the rainfall depth has been approximated with an asymptotic formula:

\[
\lambda(P) = \lambda_\infty + (1 - \lambda_\infty) \exp \left( - \frac{P}{b} \right) \tag{6}
\]

where:
- \( \lambda_\infty \): initial abstraction ratio (\( - \)) for rainfall tending to infinity,
- \( P \): rainfall depth (mm),
- \( b \): constant parameter (\( - \)).

Parameters in Equation (5) were next identified using the Table Curve 2D software [53].

3. Results and Discussion

3.1. Initial Abstraction Ratio Variation
Characteristics of the selected storm events for both catchments are summarized in Table 4. In the Służew Creek catchment, recorded rainfall depths ranged from 4.3 mm up to almost 76 mm, with the average runoff coefficient (ratio of rainfall to runoff) equal to 0.125. The estimated initial abstraction ratio ($\lambda$) for all recorded events varied from 0.002 to 0.188 and thus was lower than the original value of 0.20. The $\lambda$ average value over all 53 analyzed storm events was equal to 0.026.

In the case of the Zagożdżonka River catchment, rainfall depths varied from 5.8 mm to 145.1 mm, with the average runoff coefficient estimated as 0.106. The average initial abstraction ratio in the Zagożdżonka River catchment over all 42 storm events was equal to 0.047, which was almost twice as high as in the Służew Creek catchment but still lower than 0.20. For individual events, $\lambda$ varied from 0.001 to 0.512. Among all analyzed storm events, only for two events was $\lambda$ higher than 0.2, while for all other 40 events it was below this original value.

The values of $\lambda$ for individual events are presented in Figure 4. In the case of the Zagożdżonka River, the data are more dispersed, meaning that the variation in $\lambda$ for different storm events was higher than for the Służew Creek catchment. However, whereas the mean values varied for both catchments, the median values are similar, i.e., 0.017 and 0.018, respectively, for Służew Creek and Zagożdżonka River.

These findings demonstrate that for both catchments the initial abstraction ratio $\lambda$ varied for different storm events, and for most storm events it was lower than the original value of 0.2 suggested by the authors of [5] and often even lower than 0.05, which was proposed as a modification of the originally developed method [18]. Similar results were reported by other researchers [9,20,23], who also used a varying value for $\lambda$ in their studies. These findings suggest that using a varying value of $\lambda$ may indeed be more appropriate than a constant fixed value for all events.

**Table 4.** Characteristics of rainfall-runoff events recorded in the catchments of Służew Creek and Zagożdżonka River.

| Category                        | Abbr. | Unit | Służew Creek | Zagożdżonka River |
|---------------------------------|-------|------|--------------|------------------|
|                                 |       |      | Range        | Average          | Range       | Average       |
| No. of events                   | n     | -    | -            | 53               | -            | 42            |
| Rainfall depth                  | P     | mm   | 4.3–75.8     | 22.8             | 5.8–145.1   | 25.8          |
| Direct runoff                   | $H$   | mm   | 0.2–16.3     | 3.0              | 0.2–21.8    | 2.9           |
| Runoff coefficient              | $c = \frac{H}{P}$ | -   | 0.053–0.295  | 0.125            | 0.018–0.577 | 0.106         |
| Initial abstraction             | $la$  | mm   | 0.1–4.8      | 2.2              | 0.4–12.5    | 3.7           |
| Maximum potential catchment retention | $S$ | mm   | 23.4–683.3   | 151.3            | 9.1–1342    | 280.4         |
| Initial abstraction ratio       | $\lambda = \frac{la}{S}$ | -   | 0.002–0.188  | 0.026            | 0.001–0.512 | 0.047         |
3.2. Initial Abstraction Ratio Dependency on the Land Use Type

The Zagożdżonka River catchment with 96% of undeveloped areas (forests, meadows, arable lands) has a much higher retention capacity than does the Służew Creek catchment, where undeveloped areas cover only 35%. Thus, as the elevations of these catchments do not play any role in the runoff generation, we can conclude that the value of $\lambda$ depends on the land use type in the catchment and it decreases with an increasing ratio of the catchment imperviousness. Thus, it is logical that the value of $\lambda$ is smaller than 0.2 in the urbanized catchment of Służew Creek. It is surprising, however, that even in the Zagożdżonka catchment that has a high proportion of forests and meadows (53%) the ratio $\lambda$ did not reach the original value of 0.20.

3.3. Initial Abstraction Ratio Dependence on the Vegetation State

As it appears from our results in Section 3.2, the initial abstraction ratio can be related to the dominant land use in the catchment. Hence, its value may also change seasonally due to the state of the vegetation development. Figure 5 presents the variability of initial abstraction ratio within the three investigated seasons in both studied catchments, i.e., (I) beginning of the vegetation season (April–May), (II) full vegetation state (June–August), and (III) end of the vegetation season and plants resting period (September–March).

In the case of the Zagożdżonka River catchment a noticeable increase in the value of $\lambda$ may be noticed for the vegetation period (May–September). During the full vegetation period, rainfall depths were intercepted by plants and initial abstractions were the greatest. For the Służew Creek catchment, no relevant change in the ratio was observed and the ratio value seemed to be relatively constant over time. The small percentage of vegetation in this catchment, which is dominated by the urban area instead, probably limits the role of the interception in the runoff formation. Hence, we can conclude that the seasonal variability in the initial abstraction ratio can be observed only in a catchment where vegetation plays a role. Depending on the vegetation type and its percentage in the catchment, this factor may need to be accounted for when estimating the initial abstraction ratio in agricultural or forested catchments. No variation in the ratio should be expected in urbanized or highly impervious catchments and an average value for the ratio over all seasons could be used.
3.4. Initial Abstraction Ratio Variation with Rainfall Depth

In the case of the Służew Creek catchment, 43 storm events occurred during the summer period (May–September) and the estimated values of the initial abstraction ratio for these events have been plotted versus rainfall depths in Figure 6. Although the variability of $\lambda$ with rainfall depth was high, for rainfall depths higher than 30 mm, the initial abstraction ratio seemed to be relatively constant and varied about the value of 0.0089.

![Figure 6. Initial abstraction ratio vs. rainfall depth for summer period, Służew Creek catchment.](image)

The same procedure was repeated for the Zagożdżonka River, resulting in 32 summer events and the results are plotted in Figure 7. In this catchment, a greater variation of $\lambda$ (especially for low rainfalls) was observed than for that in the Służew Creek catchment (compare with Figure 6). Although the relationship between the initial abstraction ratio and the rainfall depth was in this catchment less pronounced, a similar tendency to the Służew Creek catchment could also be observed here, i.e., a constant value of the initial abstraction ratio approaching 0.0109 for rainfalls with the
rainfall depth higher than 20 mm may be noticed. For the case of the Służew Creek catchment, the coefficient of determination ($R^2$) equaled 0.470 and for the Zagożdżonka River catchment it was 0.236.

Estimations of similar relationships for the other two seasons were not performed due to too few events per season. The relationship between the initial abstraction and the rainfall depth, and the initial abstraction and the maximum potential retention, could not be established for recorded events (no relationship was observed).

![Figure 7. Initial abstraction ratio vs. rainfall depth for summer period, Zagożdżonka River catchment.](image)

A similar phenomenon with the equilibrium in the initial abstraction ratio was observed by Santikari and Murdoch [9] who also found that the initial abstraction amount approaches some constant value after a certain rainfall depth is exceeded. They, however, did not explore the relationship between the initial abstraction ratio and the rainfall depth itself. This phenomenon observed in our data can be explained by the fact that usually after heavy rainfalls, the entire catchment area takes part in the runoff formation. Therefore, the initial abstraction does not increase further and, consequently, the initial abstraction ratio approaches a constant value. In contrast to that, during small rainfalls, only some and often various parts of the catchment contribute to the runoff formation, causing a variation in the initial abstraction ratio. Although usually the catchment area located closest to the channel contributes most to the generated runoff during small rainfall events, the exact catchment contribution depends on the movement of the storm cloud and the detection of the rainfall cloud by local point measurements [54]. Note that the SCS method was originally designed for a direct runoff estimation of large (annual) events, during which the spatial patterns of the rainfall do not play any significant role in the runoff generation [5]. In reference to the above, Hawkins et al. [55] suggested selecting representative events in the watershed, i.e., with rainfall depths higher than 1 inch (25.4 mm), for analyses of the $CN$ parameter. In our case, we did not limit the selection of events to rainfalls exceeding this threshold value, as this would reduce the number of analyzed events to 13 in Służew Creek and 12 in Zagożdżonka River. Application of the SCS-CN method to rainfall events smaller than annual events is a common practice for runoff estimation in ungauged catchments, where other more data intensive models cannot be applied [8,15,33]. Such applications to small(er) events may, however, result in a lower model performance than that expected by the method, and the reasons for that should always be clarified.

3.5. Initial Abstraction Ratio May Change Locally

As our results from recorded storm events in two catchments of different dominant land use type showed, the initial abstraction ratio varies from storm event to storm event, and it is related to the rainfall depth. This ratio also varies seasonally and is linked to the land use type as well as the
state of the vegetation. It should also be noted that the method of la estimation applied for this study is devoted to small catchments, for which the effect of water travel time within the catchment may be neglected. The presented approach does not suit large catchments, where the effect of runoff routing and the effect of the spatial variability of rainfall on the runoff production may play a significant role. Thus, for such large size catchments, the validity of the obtained results may be limited. Hence, more research is needed on the initial abstraction ratio in different climatic regions and also for catchments with different land use types, to verify results found in our study and to compare local estimates with original values (0.2 and 0.05). We suggest that if local information is available, the initial abstraction ratio for the SCS-CN method should be estimated from locally collected data before applying the method to flood estimation or designing flood structures. Of course, estimating the value of \( \lambda \) for each event or catchment independently can be problematic in practice especially for ungauged catchments without recorded storm events. However, it should still be possible and reasonable to use an initial abstraction ratio value that is specific for the region or catchment type, if such values are available. In the case of no regional or catchment-type values being available, standard values as originally proposed in the SCS-CN method should be used instead. Such local verification is especially required if the SCS-CN method is applied outside of its original scope, i.e., to storm events smaller than annual floods. Using the originally proposed value of 0.2 for such small storm events may be linked with underestimation of the runoff amount and thus flood risk in catchments, where the estimated value of the initial abstraction ratio is much lower than its original value. If only large annual floods are of interest, we suggest using the value proposed originally, i.e., 0.2, as our results demonstrated the initial abstraction ratio may indeed produce values close to this original value under some conditions (e.g., large floods) and these conditions should be first verified locally to define the application boundaries for the original value of 0.2. For instance, one should define the return period of floods for which the original value of 0.2 or 0.05 could still be applied, and the threshold value of the return period above which local estimates are preferable.

4. Conclusions

In this work, rainfall-runoff storm events recorded in the period of 2009-2017 in two small Polish catchments of different land use types (urbanized and agroforested) were analyzed to estimate the initial abstraction ratio of the SCS-CN method and to explore its variability with rainfall depth, land use type, and season. Based on our results, the following conclusions have been made:

- Estimated values of the initial abstraction ratio varied between storm events and were most often lower than the original value of 0.20 originally suggested. For the urbanized catchment, this ratio ranged from 0.002 to 0.188, with the average value of 0.025, while for the agroforested catchment, the average ratio equaled 0.047, ranging from 0.001 to 0.512;
- The initial abstraction ratio varies over seasons, especially in the case of non-urbanized catchments with a high percentage of area covered with vegetation. Its higher value is expected during the vegetation period due to the occurrence of plants’ interception. In urbanized catchments, a variation of the ratio over seasons is expected to be small;
- For large rainfall events, the initial abstraction ratio approaches a constant value after the rainfall depth exceeds a certain threshold value. This threshold is catchment dependent and in the case of the urbanized catchment it was \( P > 30 \text{ mm} \) (\( \lambda \rightarrow 0.0089 \)) and in the case of the agroforested catchment it was \( P > 20 \text{ mm} \) (\( \lambda \rightarrow 0.0109 \));
- When using the SCS-CN method, special care should be taken to determine the initial abstraction ratio, as the suggested value of 0.20 may be too high. This may result in underestimation of the runoff depth that may have serious consequences in terms of the underestimation of flood risk.

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