Effects of different cosmic ray transport models on galaxy formation

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ABSTRACT
Cosmic rays (CRs) with \sim 10^3 GeV energies can contribute significantly to the energy and pressure budget in the interstellar, circumgalactic, and intergalactic medium (ISM, CGM, IGM). Recent cosmological simulations have begun to explore these effects, but almost all studies have been restricted to simplified models with constant CR diffusivity and/or streaming speeds. Physical models of CR propagation/scattering via extrinsic turbulence and self-excited waves predict transport coefficients which are complicated functions of local plasma properties. In a companion paper, we consider a wide range of observational constraints to identify proposed physically motivated cosmic ray propagation scalings which satisfy both detailed Milky Way (MW) and extragalactic \gamma-ray constraints. Here, we compare the effects of these models relative to simpler ‘diffusion+streaming’ models on galaxy and CGM properties at dwarf through MW mass scales. The physical models predict large local variations in CR diffusivity, with median diffusivity increasing with galactocentric radii and decreasing with galaxy mass and redshift. These effects lead to a more rapid dropoff of CR energy density in the CGM (compared to simpler models), in turn producing weaker effects of CRs on galaxy star formation rates (SFRs), CGM absorption profiles, and galactic outflows. The predictions of the more physical CR models tend to lie ‘in between’ models which ignore CRs entirely and models which treat CRs with constant diffusivity.

Key words: plasmas – stars: formation – cosmic rays – galaxies: active – galaxies: evolution – galaxies: formation.

1 INTRODUCTION
It is well-established that CRs represent a non-negligible fraction of the energy and pressure budget in the interstellar medium (ISM), and a number of recent theoretical studies incorporating CRs at dominant \sim 10^3 GeV energies in galaxy simulations have argued that CRs could significantly influence galaxy formation, primarily via their effect enhancing outflows, suppressing inflows, and changing the phase structure of the CGM around galaxies (see e.g. Jubelgas et al. 2008; Uhlig et al. 2012; Booth et al. 2013; Hanasz et al. 2013; Salem, Bryan & Hummels 2014; Girichidis et al. 2016; Pakmor et al. 2016; Simpson et al. 2016; Ruszkowski, Yang & Zweibel 2017; Wiener, Pfrommer & Oh 2017; Butsky & Quinn 2018; Farber et al. 2018; Jacob et al. 2018; Holguin et al. 2019). However, the microphysics of \sim 10^3 GeV CR transport, encapsulated in parameters like scattering rates \nu, diffusivity \kappa, or streaming speeds \nu_s remain deeply uncertain, and previous galaxy simulations have adopted extremely simple parametrizations such as assuming a constant diffusivity and/or streaming at some multiple of the Alfvén speed. In a series of papers, Chan et al. (2019), Hopkins et al. (2020c) (Papers I & II), and Ji et al. (2020) used such simplified models to argue that CRs could significantly influence galaxy formation in intermediate through Milky Way (MW)-mass haloes at low redshifts (z \lesssim 1), but that these predictions were most sensitive to the values of the CR transport parameters adopted (compared to all other CR model variations considered). Meanwhile, microphysical models for CR transport motivated by CR scattering from either extrinsic turbulent (ET) fluctuations in magnetic fields, or (in more modern models) self-confinement (SC) via gyroresonant Alfvén-waves self-excited by CR streaming motion predict that these coefficients should be non-linear, complicated functions of a number of plasma properties (see Zweibel 2013, 2017), e.g. turbulent dissipation rates ($\delta$), CR energy densities ($e_\gamma$) and their gradients; magnetic field strengths ($B$) or energies ($e_B$) or the plasma $\beta$; gas densities ($n$), temperatures ($T$), and ionization fractions ($f_{\text{ion}}$); and CR gyro radii ($R_\gamma$) or frequencies ($\Omega$).

Recently, Hopkins et al. (2020b) (H20) presented the first cosmological galaxy simulations that used CR transport coefficients taken from the more complicated scalings predicted by ET or SC models. H20 considered dozens of model variants (as well as simpler constant diffusivity or CD models), and compared each in detail to CR observations including \gamma-ray measurements from the SMC/LMC/M33/MW/M31 and nearby starburst galaxies, and MW grammage/residence time/rigidity-dependence/ionization rate/CR energy density constraints measured at the solar circle. This
showed that only a small subset of these models were observationally allowed. However this subset does differ from CD models in important ways: the transport parameters, being non-linear functions of local plasma properties, vary locally by orders-of-magnitude on sub-kpc scales in the ISM and CGM, and vary systematically with galaxy mass, redshift, and galactocentric radius in non-trivial fashion. In this letter, we explore how these differences in CR transport physics can influence galaxy properties, considering a subset of observationally allowed CD, ET, and SC models from H20.

2 METHODS

2.1 Overview

The simulations here are all presented in H20, so we briefly summarize here. The simulations are run with GIZMO\(^1\) (Hopkins 2015), with the meshless finite-mass MFM solver (a mesh-free finite-volume Lagrangian Godunov method). All simulations include ideal magnetohydrodynamics (MHD; see Hopkins & Raives 2016; Hopkins 2015), with the meshless finite-mass MFM solver (a mesh-free Lagrangian Godunov method). All simulations include 2015), with the meshless finite-mass MFM solver (a mesh-free Lagrangian Godunov method). All simulations include ideal magnetohydrodynamics (MHD; see Hopkins & Raives 2016; Hopkins 2016 for methods and tests); anisotropic Spitzer–Braginskii conduction and viscosity (see Hopkins et al. 2020c and Hopkins 2017; Su et al. 2017); and gravity with adaptive Lagrangian force softening for gas (matching the hydrodynamic resolution). These are cosmological ‘zoom-in’ runs, evolving a large box from \(z \gtrsim 100\) with resolution concentrated on a \(\sim 1–10\) Mpc comoving volume around a ‘target’ halo of interest.

Radiative cooling, star formation, and stellar feedback is included following the FIRE-2 implementation of the Feedback In Realistic Environments (FIRE) physics (details in Hopkins et al. 2018b). Cooling from 10–10\(^{10}\) K accounts for metal-line, fine-structure, photo-electric, photo-ionization, cosmic ray, dust, atomic, and molecular processes, including both local radiation sources and the meta-galactic UV background (with self-shielding); we allow star formation only in gas which is locally self-gravitating (Hopkins, Narayanan & Murray 2013; Grudić et al. 2018), self-shielding, Jeans-unstable, and dense (\(\gtrsim 1000\) cm\(^{-3}\)). Stars evolve according to standard stellar evolution tracks accounting explicitly for the mass, metals, momentum, and energy injected via individual SNe (Ia & II) and O/B and AGB-star mass-loss (see Hopkins et al. 2018a) and their radiation (including photo-electric/ionization heating and radiation pressure with a five-band radiation-hydrodynamic scheme; Hopkins et al. 2020a).

The CR treatment follows Papers I & II, which include extensive tests, as updated in H20. We evolve a single-bin (\(\sim\)GeV) or equivalently constant spectral distribution of CRs as a relativistic fluid\(^2\) (energy density \(e_{\text{cr}}\), pressure \(P_{\text{cr}} = e_{\text{cr}}/3\); e.g. McKenzie & Voelk 1982) which obeys the two-moment transport equations:

\[
\partial_t e_{\text{cr}} + \nabla \cdot \left[ \mathbf{u} (e_{\text{cr}} + P_{\text{cr}}) + \mathbf{F} \right] = \mathbf{u} \cdot \nabla P_{\text{cr}} - \Lambda_{\text{st}} - \Lambda_{\text{coll}} + S_{\text{in}}
\]

\[\frac{D_t \mathbf{F}}{c^2} + \nabla \cdot \rho_{\text{cr}} = - \frac{\mathbf{F}}{3 \kappa_{\text{e}}},\]

where \(\mathbf{u}\) is the gas velocity; \(\mathbf{F}\) the CR flux in the fluid frame; \(S_{\text{in}}\) the CR source term (determined by assuming 10 per cent of the SNe ejecta energy in each explosion goes into CRs); \(\nabla \cdot P_{\text{cr}} = \mathbf{b} \cdot \nabla P_{\text{cr}}\) is the cosmic ray pressure gradient parallel to the magnetic field \(B^3\Lambda_{\text{st}} = \min(v_{\text{st}}, v_{\text{cr}}) |\nabla P_{\text{cr}}|\) represents ‘streaming losses’ as gyro-resonant Alfven\’s waves (with Alfven speed \(v_{\text{st}}\) and unresolved wavelengths of the order of the CR gyro-radius \(r_{\text{gyro}}\)) are excited by CR streaming and rapidly damp (Wentzel 1968; Kulcsar & Pearce 1969); \(\Lambda_{\text{coll}} = 5.8 \times 10^{-6} \text{ s}^{-1} \text{ cm}^3 (n_{\text{i}} + 0.28 n_{\text{e}})\) represents collisional losses (with \(n_{\text{i}}\) the free electron number density for Coulomb losses; Guo & Oh 2008); \(\bar{\epsilon}\) is the maximum (physical or numerical) CR free-streaming/signal speed; \(\nabla \cdot \mathbf{F} \equiv \hat{F} \left[ \partial \hat{F} / \partial t + \nabla \cdot (\mathbf{u} \hat{F}) + \mathbf{F} \cdot \left( \nabla \cdot \mathbf{u} \right) \right]\) is the derivative operator derived (for a gyrotropic CR distribution function) in Thomas & Pfummer (2019); and \(\kappa_{\text{e}} = \kappa_1 + (4/3) \kappa_{\text{cr}} v_{\text{st}}\) (with \(\kappa_{\text{e}} = P_{\text{cr}}/|\nabla P_{\text{cr}}|\) the CR gradient scale length) defines the streaming/diffusive speeds. CRs influence the gas as the appropriate fraction of the streaming+hadrton+Coulomb losses are thermalized while the CR pressure appears in the gas momentum equation.

2.2 Different CR transport models

With these definitions, \(\kappa_{\parallel}\) and \(v_{\parallel}\) are the traditional CR parallel diffusivity and streaming speeds; a ‘pure diffusion’ equation for CR transport results if we take \(\bar{\epsilon} \to \infty\) (eliminating the second-moment/flux equation) with \(\kappa_1 = \text{constant}\) and \(v_{\parallel} = 0\), while a ‘pure streaming/advection’ equation results from \(\bar{\epsilon} \to 0\) with \(\kappa_1 = 0\) and \(v_{\parallel} = \text{constant}\). Other parameters in our CR model are uncertain at a more modest (factor \(\sim 2\) level, and produce only weak effects on galaxy properties: in contrast \(\kappa_{\perp}\) varies by up to \(\sim 8\) orders of magnitude in different models discussed in the literature for the MW alone (see H20) and qualitatively changes whether or not CR pressure can couple to gas at all. Here we consider only a small subset of models (summarized in Table 1) from H20 that can reproduce the CR observations. The full scalings of \(\kappa_{\parallel}\) and \(v_{\parallel}\) with plasma properties are quite complicated and are presented in full in H20, we simply summarize.

(i) Constant diffusivity (CD) models adopt \(\kappa_1 = \text{constant}\) and \(v_{\parallel} = v_{\text{Alfv}}\) (ideal MHD Alfven speed). These have no particular physical motivation, but are the most commonly adopted models in the literature and were the basis of Papers I & II (where we showed CR observations require \(\kappa_1 \sim (3 – 30) \times 10^{35} \text{ cm}^2 \text{ s}^{-1}\)).

(ii) Extrinsic turbulence (ET) models assume CR scattering from pre-existing turbulence. The most theoretically well-motivated models from H20 (‘Alfven-C00’ and ‘Fast-YL04’) produce far too-low a scattering rate (too-high \(\kappa\) ) compared to \(\sim\)GeV CR observations, which likely indicates that self-confinement dominates \(\sim\)GeV CR scattering. To explore the somewhat uncertain turbulent scattering physics, H20 did consider variant ET models that involved

\[3\text{We neglect perpendicular diffusion, as it is expected to be smaller by orders of magnitude (powers of the ratio of the gyro radius to CR mean free scattering length; see e.g. Rodrigues et al. 2019).}\]
Table 1. Summary of CR transport models from H20 (Section 2.2) considered here. All models include star formation, stellar feedback, MHD, anisotropic conduction/viscosity, and all (except ‘SC:Default’ included for reference) produce γ-ray signatures consistent with observations across SMC-through-starburst galaxies, and similar MW grammage/residence time/energy density at the solar circle.

| Name | Description |
|------|-------------|
| CD: | Constant-Diffusivity (CD) Models: constant κ_j = κ_j 10^{29} cm^2 s^{-1}, with streaming v_{dr,1} = v_A = v_A^{\text{ideal}} = (|B|^2/4\pi\rho)^{1/2} |
| κ_29 = 3 | κ_29 = 3, v_{dr,1} = v_A: lowest-κ_j observationally-allowed constant-κ model from Papers I & II |
| κ_29 = 30 | κ_29 = 30, v_{dr,1} = v_A: highest-κ_j observationally-allowed constant-κ model from Papers I & II |
| ET: | Extrinsic Turbulence (ET) Models: κ_j = \mathcal{M}_A^2 c \ell_{\text{turb}} f_{\text{turb}} with different f_{\text{turb}} and \ v_{dr,1} = 0 \ (\text{turbulent scale } \ell_{\text{turb}}, \text{Alfvén Mach } \mathcal{M}_A) |
| Alfven-Max | f_{\text{turb}} = 1: Alfven-wave scattering in a GS95 cascade ignoring gyro-averaging and anisotropy terms (otherwise f_{\text{turb}} \gtrsim 1000) |
| Fast-Max | Fast-mode scattering, neglecting ion-neutral and β > 1 viscous damping (otherwise f_{\text{turb}} \gtrsim 10^3) |
| SC: | Self-Confinement (SC) Models: κ_j = c \ell_{\text{turb}} (16/3\pi) (\ell_{\text{turb}}/\ell_{\text{iso}}) (\ell_{\text{turb}}/\ell_{\text{iso}}) f_{\text{QLT}} f_{\text{turb}} (\text{SC:Default}) from gyro-resonant damping Γ, v_{dr,1} = v_{\text{iso}} = \mathcal{V}_{\text{iso}} A_{\text{iso}}^{1/2} |
| f_{\text{QLT}} = 100 | f_{\text{QLT}} = 100 with Γ = Γ_{\text{iso}} + Γ_{\text{turb}} + Γ_{\text{LL}} + Γ_{\text{NL}} (\text{ion-neutral, turbulent, linear and non-linear Landau damping all included}) |
| ‘Default’ | as above with f_{\text{QLT}} = 1 (simplest SC model; observationally disfavoured by γ-ray flux+grammage – listed for reference) |
| Combined Self-Confinement & Extrinsic-Turbulence (SC+ET) Models: κ_j^{-1} = \sum κ_j^{-1} (\text{sum scattering rates}), v_{dr,1} = v_{\text{iso}} |
| SC+ET | ‘Default’ scattering from Alfvénic (ET:Alfvén-C00) + fast (ET:Fast-YL04) modes + SC with 100x larger Γ_{\text{turb}} (SC:fc=100) |

either ignoring gyro-averaging effects from anisotropy^4 (model ‘Alfvén-Max’), or ignoring some fast-mode damping terms (model ‘Fast-Max’). These, although poorly motivated theoretically, provide a useful reference because the dimensional scaling of κ resembles that of the most well-motivated models. This scaling, which, for ‘Alfvén-Max,’ is κ_j \sim \mathcal{M}_A^2 c \ell_{\text{turb}} f_{\text{turb}} (with Alfvén Mach number \mathcal{M}_A on turbulent length scale \ell_{\text{turb}}), shows that κ_j should be expected to increase at large radii due to the increase in turbulent length scales. Other effects, which are absorbed in f_{\text{turb}} and included in other turbulence models (e.g. f_{\text{turb}} \sim 30 \mathcal{M}_A^2 Re^{-1/2} in the simplest regime for ‘Fast-Max,’ where Re is the Reynolds number), do not change this expectation.

(iii) Self-confinement (SC) models assume CRs are scattered due to self-excited gyro-resonant Alfvén-waves, and so depend on gas and CR parameters differently from ET models. H20 showed that the simplest, theoretically well-motivated SC models (e.g. the model ‘SC:Default’ in Table 1) tend to overpredict scattering rates (underpredict κ_j) by a factor \sim 100. The discrepancy with theoretical expectations could be accounted for by a number of significant uncertainties in SC physics (see Section 5.2 of H20); we therefore consider both this and the models from H20 which adopt the quasi-linear ‘correction factor’ f_{\text{QLT}} = 100 to match observations. The dependence of κ_j on plasma properties is complicated in these models (see Table 1), and depends on ionization fraction f_{\text{iso}} e_c, and \ ξ_e = e_c/|\nabla e_c|, and damping rates Γ of gyro-resonant modes from a variety of sources (see H20 for details): if e_c turbulence dominates damping (Γ \approx Γ_{\text{turb}}), then κ_j \propto ξ_e e_c^{1/2} |\nabla y_{\text{turb}}|^{1/2} \rho^{3/4} \ell_{\text{turb}} f_{\text{QLT}} f_{\text{turb}}. In general because κ_j \propto \ell_{\text{turb}} e_c, in SC, the falloff of e_c (and increase in \ ξ_e) with (spherical) galactocentric radius generally produce rising κ_j.

(iv) Combined ‘SC+ET’ models assume scattering rates from SC and ET models, adopting the Alfvén-C00 and Fast-YL04 models above and (for the sake of contrast) a slightly different SC model with the ‘quasi-linear’ correction applied to the turbulent damping rate Γ_{\text{turb}} as compared to the total Γ or κ_j (as in f_{\text{QLT}} = 100).

^4Per Chandran (2000), the ‘anisotropy’ referred to here in the context of models like ‘Alfvén-Max’ is the anisotropy of the Alfvénic modes in the extrinsic turbulent cascade at small (gyro-resonant) scales, which is predicted to be substantial in any scenario which exhibits critical balance (e.g. a Goldreich & Sridhar 1995-type cascade). The CRs themselves assumed to be nearly isotropic.

3 RESULTS

3.1 Effects on the CGM

Fig. 1 illustrates the key differences between the allowed models in the CGM. We compare these haloes (a representative dwarf, intermediate, and massive system from H20), at z = 0, with the CR models from Table 1, and a reference ‘No CRs’ model which does not include CRs. We measure the angle-averaged (isotropic-equivalent) mean CR scattering-rate-weighted diffusivity κ_eff = \int (|\nabla \Phi|/|\nabla \Phi|) d\sigma (with weight \ σ = (e_c/κ_j)^2 d^3/|\nabla (e_c/κ_j)|) x), the ratio of the CGM radial pressure gradient to the inward gravitational force, and CGM gas density and temperature in radial annuli.

H20 studied the diffusivities κ_eff and transport parameters in detail – showing for example that the ET/SC models plotted here produce order-of-magnitude local variations in κ_j that in turn mean the diffusivity weighted by scattering rate or volume or other parameters can be quite distinct. Here, what is notable is how the diffusivities tend to increase with r outside the galaxy. Recall, all models here are constrained to reproduce the same CR observations (γ-ray luminosities, grammage, residence/decay times, etc.) – but these observables are entirely dominated by gas within the central \lesssim 10 kpc around the galaxy. As a result, the allowed models tend to reproduce similar scattering-weighted mean κ in the ISM (at least for some MW-mass systems) but extrapolate differently. The SC/ET models show κ rising with r, as n_i |B|, \ δV_{\text{turb}}/\ell_{\text{turb}}, and other relevant quantities which drive CR scattering decrease. Interestingly, because the SC models feature a more sharply rising κ_eff outside the galaxy, the model ‘SC:Default’ from H20 (with f_{\text{QLT}} = 1, so κ_eff is systematically lower by a factor \sim 100 compared to ‘SC:fc=100’), while it gives very low κ_eff within the galaxy (in potential tension with observations), gives quite similar κ_eff in the CGM to the ET models considered here.

In Paper II, we show that in steady state with some fixed CR injection rate in the galaxy \dot{E}_g, neglecting losses (as the γ-ray observations require weak losses for the galaxies here), the CR pressure in the CGM must scale as \ P_{\gamma} \sim E_g/(12\pi κ_eff r). Thus, the higher-κ outside the galaxy in SC/ET models leads to lower \ P_{\gamma} which in turn means a lower gas density \rho \sim |\nabla P_{\gamma}|/|\nabla \Phi| can be supported by CR pressure against gravity (set primarily by the dark matter). As a result we see either (i) gas fails to be supported by CRs (|\nabla P_{\gamma}|/|\nabla \Phi| \ll 1) or (ii) lower CGM gas densities (smaller...
Figure 1. Properties of galaxies m11i (SMC-mass dwarf with halo virial mass $M_{\text{vir}} \sim 7 \times 10^{10} M_\odot$, mass resolution $\Delta m = 7000 M_\odot$), m11f (late-type galaxy, intermediate surface-density, $M_{\text{vir}} \sim 5 \times 10^{11} M_\odot$, $\Delta m = 12000 M_\odot$), m12i ($\sim L_\ast$ galaxy in massive halo, higher surface-density; $M_{\text{vir}} \sim 1.4 \times 10^{12} M_\odot$, at lower resolution $\Delta m = 56000 M_\odot$) with different CR transport models (Table 1), restricted to an ‘observationally allowed’ subset (plus ‘No CRs,’ for reference), at $z = 0$, measured in spherical radial annuli at $r$. Top: ‘Effective’ angle-averaged, mean scattering-rate weighted diffusivity $\kappa_{\text{eff}}$ (shaded shows inter-quartile range). Second: Volume-averaged ratio of outward CR pressure force $\nabla P_{\text{cr}}$ to gravitational force $\rho \nabla \Phi$. Third: Volume-averaged gas density $n_H$. Bottom: Volume-averaged gas temperature $T$. The qualitative effect of CRs is identical in all cases: the additional CR pressure supports much cooler gas (it does not need to be at the virial temperature), and the additional effect of CR-driven outflows reduces CGM densities (by a small factor). In ET/SC models, $\kappa_{\text{eff}}$ varies locally (by $\geq$ 1 dex) but is similar to the allowed CD models within the disc (where direct CR observations exist) for a subset of the galaxies, but tends to increase with $r$ outside the disc and can increase in other galaxies. This leads to lower CR pressures in the CGM, as (in steady state) $P_{\text{cr}} \propto \kappa_{\text{eff}} \propto \frac{1}{\kappa_{\text{eff}}}$. This in turn reduces the effects of CRs relative to the CD models.
n) appear when $\kappa_{\text{eff}}$ is larger outside the galaxy. Paper II also shows that effects of CRs in the CGM become weaker in low-mass haloes, as CR pressure (given much lower star formation rates) is less able to support the halo gas (lower $\nabla P_{\text{CR}}/|\rho \nabla \Phi|$), producing overall weaker effects of CRs in m111.

Ji et al. (2020) further explored the CGM properties of the $\kappa_{29} = 3$ runs here in detail. They showed that for runs m11f and m12f, where CRs in this run dominate the pressure support against gravity, gas at relatively low temperature $T$ can be supported, while in the ‘No CRs’ run, the dominant pressure support is thermal, requiring the gas have temperature of the order of the virial temperature (or else it falls on to the galaxy and is accreted rapidly). This leads directly to different CGM temperatures in Fig. 1, which in turn translates to different metal ionization states (with the cooler CGM in the $\kappa_{29} = 3$ run primarily photoionized, and the hotter CGM in the ‘No CRs’ run collisionally ionized) and therefore different equivalent widths in common CGM metal absorption lines. We see that with higher CGM diffusivities, the SC/ET models generally produce results ‘in between’ the CD and ‘No CRs’ models here. For this reason noted above, SC models from H20 with lower $f_{\text{QLT}} \sim 1$, for this reason, end up close to the ‘Alfvén-Max’ or ‘Fast-Max’ models in the CGM properties in Fig. 1.

### 3.2 Effects on galaxy evolution and the ISM

Fig. 2 examines the effects of different CR transport models on galaxy evolution (comparing to a baseline simulation with no CRs). This is the main focus of Papers I & II, which explore a much wider variety of galaxy properties, for constant-diffusivity models. However Paper II shows that almost all of the effects of CRs are strongly correlated because the effect of CRs is primarily as a ‘preventive’ feedback agent, contributing to CGM pressure and slowly accelerating outflows, preventing cool gas from more-rapidly accreting on to the galaxy. Thus to the extent that CRs suppress the SFRs/stellar masses in galaxies, they also modify the galaxy morphology, metallicities, angular momentum content, ISM phases, rotation curves, etc, but simply ‘moving along’ the correlations of these quantities with galaxy stellar mass and/or SFR. We therefore restrict in Fig. 2 to cosmological SFRs, the buildup of stellar mass, and galaxy rotation curves (concentration, creation of ‘cores,’ etc).

Paper II showed that the range $\kappa_{29} \sim 3$–30 favoured by $L_\gamma$ observations is also the range of $\kappa$ which produces the maximal effect of CRs on intermediate-through-MW mass systems here. At much lower-$\kappa$, CRs lose all their energy collisionally, so provide no pressure and do essentially nothing to the galaxy. At much higher-$\kappa$, CRs simply ‘escape’ and produce negligible pressure/coupling to gas. At the ‘sweet spot’ in $\kappa$, CRs from SNe can reduce SFRs by as much as a factor $\sim 5$ near $z \sim 0$, and stellar masses by factors $\sim 2$–4, acting primarily at low redshifts/late times (as shown in Paper II). However, we find that in the more physically motivated SC and ET models, the effects of CRs on galaxy evolution are weaker. They are still appreciable, but almost always lie ‘between’ the ‘No CRs’ and ‘Constant Diffusivity’ models. For the reasons above, with its intermediate diffusivity in the CGM, the reference model ‘SC:Default’ with $f_{\text{QLT}} \sim 1$ produces results similar here to the intermediate models, closes to ‘Fast-Max’ in m11i and m11f and to ‘SC+ET’ in m12i. This follows naturally from the arguments above: if the diffusivity rises with galactocentric radius in these models, the CR pressure drops more rapidly, so CRs are less efficient at re-accelerating winds and suppressing accretion on to galaxies, compared to constant-diffusivity models.

As noted, we do not explicitly consider ISM properties here, though they will be studied in much greater detail comparing the effects of some of the CR models here in Chan et al. (in preparation) and Benincasa et al. (in preparation). To leading-order, the effects of CRs shift galaxies ‘along’ a sequence via their effects in the CGM, changing the baryonic mass of the galaxy. But also recall that these models are all calibrated to reproduce a similar set of observational constraints including $\gamma$-ray luminosities and grammage and CR energy density at the solar circle in MW-like galaxies. As a result, properties like the diffusivity and CR pressure are, by construction, quite similar in the disc mid-plane. While the models predict quite distinct variations across different phases, since they have similar ‘mean’ behaviour, these generally produce second-order differences.

### 4 CONCLUSIONS

We consider for the first time the effect on galaxy and CGM properties of different physically motivated CR transport models including diffusion and streaming coefficients that vary with local plasma properties (motivated by microphysical CR transport models), in fully cosmological, multiphase ISM/CGM galaxy formation simulations. All the models here are constrained to reproduce similar CR observables including $\gamma$-ray luminosities of dwarf, MW-like, and starburst galaxies, MW grammage and residence time and CR energy density/ionization rate constraints (H20). However these observations only significantly constrain CR transport coefficients within the galactic ISM and innermost CGM (radii $\lessapprox 10$ kpc).

In the physically motivated models, there are large local variations in the ‘effective’ CR diffusivity $\kappa_{\text{eff}}$, and $\kappa_{\text{eff}}$ tends to increase significantly in the CGM, because CR scattering rates decrease in the lower density, higher-$\beta$ gas. This increasingly rapid CR diffusion leads to a more rapidly decreasing CR pressure as a function of galactocentric radius $r$, which limits the range of CGM/IGM radii over which CRs can contribute significantly to supporting gas against gravity (relative to models with a constant CR diffusivity). That, in turn, means CRs produce weaker effects on CGM phase structure, density and temperature profiles, outflow reacceleration, and suppression of galactic star formation. As a result, in all galaxy and CGM properties examined here or in Papers I & II, and Ji et al. (2020), the qualitative effects of CRs are similar, but the physically motivated CR transport models tend to produce quantitative effects in-between our runs without CRs and our favoured ‘constant diffusivity’ runs. This suggests the effects of CRs on galaxy formation, while not negligible, are relatively modest, altering galaxy masses by factors up to $\sim 2$–3, and temperatures in the CGM around $\sim L_\gamma$, low-redshift galaxies by factors up to $\sim 2$–5.

The major caveat of this study is the uncertainty regarding the true microphysical CR transport model. We showed in H20 that the models here are observationally allowed, but not unique. Moreover, our conclusion in H20 was that neither ET nor SC models can reproduce all relevant CR observations with their simplest ‘default’ parametrizations, but that they require some modifications in order to fit the observations. For example, the SC model we consider here scales the scattering rate by the arbitrary factor $f_{\text{QLT}} \sim 100$, which is necessary in order to avoid overconfining CRs in the ISM. However, these modifications (required to match observations) are not necessarily well-understood theoretically, and it is possible that they could also vary systematically with radius. If the ‘correct’ $f_{\text{QLT}}$ were not constant but instead $\sim 100$ inside the galactic disc (or even within just certain parameter space regimes relevant for $\gamma$-ray production in our simulations) and decreased with $\propto 1/r$ outside the disc, then the SC model here would still reproduce observations, but
Figure 2. Galaxy properties for m11i, m11f, m12i. Top: Star formation (SF) history (averaged in 100 Myr bins) of the galaxy, versus cosmic time. Middle: Stellar mass inside the virial radius versus scale-factor \((a = 1/(1+z))\), with \(z = 0\) value shown (number). Bottom: Circular velocity \(V_c^2 \approx GM_{\text{enc}}(<r)/r\) versus (spherical) galactocentric radius \(r\) at \(z = 0\). In all cases, CRs suppress SF at \(z \lesssim 1-2\) in these galaxies. Constant-diffusivity models tend to overestimate this suppression relative to ET or SC models, as (per Paper II) CR feedback is primarily ‘preventive’ via suppressing CGM inflows.

with a diffusivity much more weakly dependent on galactocentric radius \(r\), thus more closely resembling the ET or CD models. Our hope is that the combination of CGM, galaxy, and direct CR observations may better constrain these parameters in the future, and (in the meantime) these different results allow us to better understand the dominant systematic uncertainties in theoretical models that attempt to predict the effects of CRs on galaxy formation.

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DATA AVAILABILITY STATEMENT

The data supporting the plots within this article are available on reasonable request to the corresponding author. A public version of the GIZMO code is available at http://www.tapir.caltech.edu/~phopkins/Site/GIZMO.html. Additional data including simulation snapshots, initial conditions, and derived data products are available at http://fire.northwestern.edu.

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