Hadronic decays of the highly excited $2D_s$ resonances

Jing Ge$^{1*}$, Dan-Dan Ye$^{1,2}$ and Ailin Zhang$^1$ †

1 Department of Physics, Shanghai University, Shanghai 200444, China
2 College of Mathematics, Physics and Information Engineering, Jiaxing University, Jiaxing 314001, China

Hadronic decays of the highly excited $2D_s$ resonances have been studied in the $^3P_0$ model. Widths of all possible hadronic decay channels of the $2D_s$ have been computed. $D_{s1}^*(2700)$, $D_{s1}^*(2860)$, $D_{s3}^*(2600)$, $D(2600)$ and $D(2750)$ can be produced from hadronic decays of the $2D_s$, and relevant hadronic decay widths have been particularly paid attention to. The hadronic decay widths of $2D_s$ to $D(2600)$ or $D(2750)$ may be large, and the numerical results are different in different assignments of $D_{s1}^*(2860)$ and $D_{s3}^*(2750)$. The hadronic decay widths of $2D_s$ to $D_{s1}^*(2860)$, $D_{s3}^*(2860)$ or $D_{s1}^*(2700)$ are very small, and different in different assignments of $D_{s1}^*(2700)$.

PACS numbers: 13.25.Ft
Keywords: Hadronic decay, $^3P_0$ model

I. INTRODUCTION

The properties of highly excited heavy-light meson states have been studied for a long time, the S-wave and P-wave $D$ and $D_s$ resonances are believed established. In recent years, more and more heavy-light resonances such as the higher excited $D_s$ have been observed. However, some candidates of these highly excited heavy-light resonances have not been definitely pinned down.

$D_{s1}^*(2700)$ was first observed by Belle $[1]$ in $B^+ \rightarrow D^0 D_{s1} \rightarrow D^0 D^0 K^+$. It was also observed by BaBar in $D^+ K$ channel $[2]$. This state is included in PDG $[3]$ with $M = 2709 \pm 4$ MeV, $J^P = 1^-$ and $\Gamma = 117 \pm 13$ MeV.

$D_{s1}^*(2860)$ was first reported by BaBar $[2]$ in $D_{s1}(2860) \rightarrow D^0 K^+ D^0 K^0_s$ with a mass $M = 2856.6 \pm 1.5$ (stat)$\pm 5.0$ (syst) MeV and a width $\Gamma = 48 \pm 12$ (stat)$\pm 10$ (syst) MeV. It was observed once again in the $D^+ K$ channel $[2]$. This state is included in PDG $[3]$ with $M = 2863.2^{+4.9}_{-2.9}$ MeV, $\Gamma = 58 \pm 11$ MeV and unknown $J^P$.

Recently, LHCb collaboration reported that the resonance $m(D^0 K^0_s) \approx 2.86$ GeV contain both spin-1 and spin-3 components $[4, 5]$. These two states, $D_{s1}^*(2860)$ and $D_{s3}^*(2860)$, are suggested to be the $J^P = 1^-$ and $J^P = 3^-$ members of the $1^D$ family. In addition, two new charmed states, $D(2600)$ and $D(2750)$, were observed by BaBar Collaboration $[6, 7]$.

$D_{s1}^*(2700)$ was supposed the first radially excited $S$-wave states $D_s(2^3S_1)$. $[8, 9]$ or their mixture $[10, 11]$. Similarly, $D_{s1}^*(2860)$ was once suggested as the $J^P = 0^+$ $[12, 13]$, $J^P = 3^-$ $[12, 13, 14]$ excited $D_s$ or the orthogonal partners of $D_{s1}^*(2700)$ $[15, 16, 17]$. The $0^+$ possibility is subsequently excluded by the observation of $D_{s1}^*(2860) \rightarrow D^0 K^+$ channel. Recent experiment suggests that there are in fact two $D_{s1}^*(2860)$ and $D_{s3}^*(2860)$ close to $D_{s1}^*(2860) \pm$ $[18, 19]$, where $D_{s1}^*(2860)$ and $D_{s3}^*(2860)$ are suggested to be the $J^P = 1^-$ and $J^P = 3^-$ members of the $1^D$ family $[10, 11, 12]$.

$D(2600)$ is observed and suggested to be the first radially excited S-wave states $D(2^3S_1)$ through an analysis of their masses and helicity-angle distribution, while $D(2750)$ is observed and suggested the orbital excited $1D$ state $[20]$. In Ref. $[18, 19]$, $D(2600)$ is suggested as an admixture of $2^3S_1$ and $1^3D_1$ with $J^P = 1^-$, and $D(2750)$ is interpreted as an orthogonal partner of $D(2600)$ or $1^3D_3$. In Ref. $[10]$, $D(2600)$ was interpreted as a pure $2^3S_1$ state from its hadronic decays in the heavy quark symmetry theory. In Ref. $[20]$, an analysis of the assignment of $D(2600)$ to the first radial excitation of $D^*$ has been done in detail in an effective Lagrangian approach.

There are different interpretations to these resonances. Obviously, the nature of these resonances have not been understood clearly. In literatures, the arrangements of these resonances are mainly based on the study of their $J^P$ quantum numbers, masses and strong decay modes.

It is well known that the study of productions of these resonances is also an important way to understand them. $D_{s1}^*(2700)$, $D_{s1}^*(2860)$, $D_{s3}^*(2860)$, $D(2600)$ and $D(2750)$ can be produced from the strong decays of highly excited resonances. It will be interesting to study the hadronic production of $D_{s1}^*(2700)$, $D_{s1}^*(2860)$, $D_{s3}^*(2860)$, $D(2600)$ and $D(2750)$ from higher excited resonances. In fact, some highly excited $D_s$ resonances have been observed by BaBar, LHCb et al., more and more highly excited $D_s$ resonances are expected to be observed by these Collaborations. For kinematical reason, these resonances can be produced from hadronic decays of $2D_s$. Unfortu-
nately, the strong decays of the highly excited $2D_Ds$ resonances have seldom been studied before. In this paper, the hadronic decays of these $2D_Ds$ resonances will be studied in the $^3P_0$ model.

The paper is organized as follows. In Sec.II, we give a brief review of the $^3P_0$ model and possible decay modes of the $2D$ resonances. In Sec. III, we present the formula and numerical results of the hadronic decay of the $2D_Ds$ resonances, and the decays with $D^{*+}_s(2700), D^{*+}_s(2860), D^{*+}_s(2950), D(2600)$ or $D(2750)$ involved in the final states are particularly paid attention to. Finally, the conclusions and discussions are given in Sec. IV.

II. $^3P_0$ Model and Possible Decay Modes of the $2D_Ds$ Resonances

$^3P_0$ model is popularly known as a quark-pair creation (QPC) model, which has been extensively applied to the calculation of the OZI-allowed strong decay of meson A to meson B and C. The model was first proposed by Micu [21], and then developed by Yaouanc et al [22–24]. The decay process is shown in Fig. 1 [25, 26], where a pair of quarks $q\bar{q}$ with $J^P_C = 0^+$ are created from the vacuum and regroup with the $q\bar{q}$ within the initial meson A into two outgoing mesons B and C.

![Diagram](https://via.placeholder.com/150)

FIG. 1: Decay process of $A \rightarrow B + C$ in the $^3P_0$ model.

In $^3P_0$ model, the hadronic decay width of $A \rightarrow BC$ is

$$\Gamma = \pi^2 \left| \frac{\vec{K}}{M_A} \right|^2 \sum_{JL} |M^{JL}|^2$$

(1)

where the momentum of the daughter meson in the initial meson A’s center of mass frame is

$$|\vec{K}| = \sqrt{\left|m_A^2 - (m_B - m_C)^2\right|^2 + \left|m_A^2 - (m_B + m_C)^2\right|^2}$$

(2)

and $M^{JL}$ is the partial wave amplitude of $A \rightarrow BC$. In terms of the Jacob-Wick formula [27], the partial wave amplitude can be obtained from the helicity amplitude $M^{JL}$ where

$$M^{JL}(A \rightarrow BC) = \frac{\sqrt{2L + 1}}{2L + 1} \sum_{M_{JL}M_{JC}} \langle L0JM_JA | A M_{JL} \rangle \times \langle JBM_JB JC M_{JC} | J M_{JA} \rangle \times M^{M_{JA}M_{JB}M_{JC}}(\vec{K})$$

(3)

with $J = J_B + J_C, J_A = J_B + J_C + \vec{L}$ and $M_{JA} = M_{JB} + M_{JC}$. In this equation, the helicity amplitude

$$M^{M_{JA}M_{JB}M_{JC}} = \sqrt{8E_A E_B E_C} \gamma \sum_{M_{LA}M_{SA}M_{SB}} \langle L_A M_{LA} S_A M_{SB} | J M_{JA} \rangle$$

$$\times \langle L_B M_{LB} S_B M_{SB} | J_B M_{JB} \rangle \langle L_C M_{LC} S_C M_{SC} | J_C M_{JC} \rangle$$

$$\times \langle 1m; -1m|00\rangle \langle \chi^{13}_{SBM_{SB}} \chi^{24}_{SM_{SC}} | \chi^{12}_{SM_{SA}} \chi^{34}_{-m} \rangle$$

$$\times \langle \vec{r}_B \vec{r}_C \gamma | \vec{r}_A \gamma \rangle M^{M_{LA}M_{LB}M_{LC}}(\vec{K})$$

(4)

where the spatial integral $I_{M_{LB}M_{LC}}(\vec{K})$ is

$$I_{M_{LB}M_{LC}}(\vec{K}) = \int d\vec{k}_1 d\vec{k}_2 d\vec{k}_3 d\vec{k}_4$$

$$\times \delta^3(\vec{k}_1 - \vec{k}_2 - \vec{p}_A) \delta^3(\vec{k}_3 + \vec{k}_4) \times \delta^3(\vec{p}_B - \vec{k}_1 - \vec{k}_3) \delta^3(\vec{p}_C - \vec{k}_2 - \vec{k}_4)$$

$$\times \Psi_{nLBM_{LB}}^*(\vec{k}_1, \vec{k}_3) \Psi_{nLCLM_{LC}}(\vec{k}_2, \vec{k}_4)$$

$$\times \Psi_{nLAM_{LA}}(k_1, k_2) \Psi_{nLAM_{LA}}^*(k_3, k_4)$$

$$\times \left( \frac{\vec{k}_3 - \vec{k}_4}{2} \right)^2$$

(5)

The details of the indices, matrix elements and other indications are given in Ref. [26].

With these formula in hand, we go ahead with our calculation. In the calculation, the simple harmonic oscillator (SHO) wave function is employed to represent the meson wave function. The meson flavor functions follow the convention in Ref. [28]: $D^0 = c\bar{u}, D^+ = -c\bar{d}, D^+_s = -c\bar{s}, K^+ = -u\bar{s}, K^- = s\bar{u}, \phi = -s\bar{s}, \eta = (u\bar{u} - d\bar{d})/2 - s\bar{s}/\sqrt{2}$ and $\eta' = (u\bar{u} - d\bar{d})/2 + s\bar{s}/\sqrt{2}$.

For the parameters involved in $^3P_0$ model, the light nonstrange quark pair creation strength $\gamma$ and the strange quark pair creation strength $\gamma_{s\bar{s}}$ are correlated by $\gamma_{s\bar{s}} \approx \gamma/\sqrt{3}$ [23] with $\gamma = 7.85$ [29]. The constituent quark masses are taken to be $m_u = 1.43$ GeV, $m_d = m_d = 0.45$ GeV and $m_s = 0.55$ GeV [17]. The resonance masses and the effective scale parameters $\beta$ for different resonances used in our calculation are listed in Table. 1 [8] and Table. 2 [17], respectively. There is not a $2D_Ds$ observed, and the masses of these resonances are unknown. In our calculation, theoretical predicted masses of the $1^– 2^1D_1 D_s (3383 \text{ MeV})$ and the $3^– 2^3D_3 D_s (3469$
MeV \[30] are employed, respectively. For the $2^- D_s$ resonance, $2^3 D_2$ may mix with $2^1 D_2$, which may result in a complicated mixing. Only when the detail of the mixing is clear, can we give the hadronic decay widths of each $2^-$ resonances. In this paper, we give only the results of pure $2^3 D_2$ and $2^1 D_2$. As an approximation, the average mass (3429.5 MeV) of the two predicted $2^- D_s$ in Ref. 30 is taken as the mass input of $2^3 D_2$ and $2^1 D_2$.

Possible kinematically allowed decay modes of these four $2D_0$ $D_s$ resonances are presented in Table. 3 and Table. 4.

### III. HADRONIC DECAYS OF $2D_0$ $D_s$ RESONANCES

Possible hadronic decay modes and their numerical decay widths of $D_s(2^{3} D_1)$ and $D_s(2^{3} D_3)$ except for final states including $D_s^*(2700)$, $D_{s1}(2860)$, $D_{s3}(2860)$, $D(2600)$ or $D(2750)$ are shown in Table. 5. Similar results of the strong decays of $D_s(2^{3} D_2)$ and $D_s(2^{1} D_2)$ are shown in Table. 6.

In our calculation, $D_s(2430)$ and $D_{s1}(2460)$ are assigned as the $1^+(j^P = \frac{1}{2}^+)$ $D$ and $D_s$, respectively.

| TABLE I: Meson masses used in our calculation (MeV). |
|---|
| States | Mass |
| $K^0$ | 493.677 |
| $K^0$ | 497.614 |
| $K^{*0}$ | 891.66 |
| $K^{*0}$ | 896 |
| $\eta$ | 547.853 |
| $\eta'$ | 957.78 |
| $\phi$ | 1019.455 |
| $D^{\pm}$ | 1869.2 |
| $D^0$ | 1864.84 |
| $D^{*\pm}$ | 2010.27 |
| $D^*$ | 2006.97 |
| $\Lambda_s$ | 1968.49 |
| $\Sigma_s$ | 2112.3 |
| $\Lambda_{s0}(2317)$ | 2317.8 |
| $\Lambda_{s1}(2460)$ | 2459.6 |
| $\Lambda_{s3}(2536)$ | 2535.35 |
| $D_{s0}(2573)$ | 2571.9 |
| $D_{s1}(2700)$ | 2709 |
| $D_{s3}(2860)$ | 2859 |

| TABLE II: Different $\beta$ values for the S-wave, P-wave and D-wave resonances in MeV. |
|---|---|---|---|---|
| $n^{2S+1} L_J$ | $u\bar{u}$ | $u\bar{s}$ | $s\bar{s}$ | $c\bar{u}$ | $c\bar{s}$ |
| $1^1 S_0$ | 470 | 466 | 470 | 453 | 484 |
| $2^1 S_0$ | 294 | 301 | 310 | 325 | 343 |
| $1^3 S_1$ | 308 | 322 | 338 | 379 | 406 |
| $2^3 S_1$ | 258 | 267 | 279 | 306 | 324 |
| $1^1 P_1$ | 280 | 290 | 302 | 328 | 348 |
| $2^1 P_1$ | 247 | 255 | 265 | 287 | 303 |
| $1^3 P_1$ | 284 | 294 | 306 | 332 | 352 |
| $2^3 P_1$ | 250 | 259 | 269 | 290 | 306 |
| $1^1 D_J$ | 261 | 270 | 281 | 304 | 321 |
| $2^1 D_J$ | 238 | 246 | 255 | 275 | 290 |
| $1^3 D_J$ | 261 | 270 | 281 | 304 | 321 |
| $2^3 D_J$ | 238 | 246 | 255 | 275 | 290 |

$D_s(2420)$ and $D_{s1}(2536)$ are assigned as the excited $1^+(j^P = \frac{3}{2}^+)$ $D$ and $D_s$. Through the relation between the $j^P$ eigenstates and the $2S+1 L_J$ eigenstates, these two $1^+$ resonances are regarded as a mixture of $1^1 P_1$ and $1^3 P_1$ resonances

\[
\left( |1^+, j^P = \frac{1}{2}^+ \rangle \right) = \left( \begin{array}{c} \cos \theta \\ \sin \theta \end{array} \right) \left( \begin{array}{c} |1^1 P_1 \rangle \\ |1^3 P_1 \rangle \end{array} \right)
\]

where the mixing angle $\theta = -\tan^{-1}\sqrt{2} = -54.7^\circ \ [20, 30].$

For a particular $J$, the larger the angular momentum ($L$) between the two final states, the smaller the corresponding $M_{JL}$. However, for a particular decay channel, both $J$ and $L$ could vary, and there is not an one-to-one relation between the decay width and the $M_{JL}$. From the numerical results in Table. 5, the dominant decay modes of $D_s(2^{3} D_1)$ are $D(2430)K$, $D^*K_{1}(1270)$ and $D^*K(1410)$ et al, while the dominant decay modes of $D_s(2^{3} D_3)$ are $DK_{1}(1270)$, $D^*K^*(1410)$ and $D^*K_{2}(1430)$ et al. From the numerical results in Table. 6, the dominant decay modes of $D_s(2^{3} D_2)$ are $D^* K$, $D^* K_{1}(1270)$ and $D^* K(1410)$ et al, while the dominant decay modes of $D_s(2^{3} D_2)$ are $D^* K^*(1410)$, $D^* K_{1}(1400)$ and $D^* K$ et al. In forthcoming experiments, the $2D_0$ $D_s$ resonances are expected to be observed in these dominant hadronic decay channels.

Since there are different assignments to $D_{s1}(2700)$, $D(2600)$ and $D(2750)$, their hadronic productions (together with the production of $D_{s1}(2860)$ and $D_{s3}(2860)$) from $2D_0$ $D_s$ resonances are studied independently in the following subsection.
TABLE III: OZI-allowed hadronic decay modes of $D_s(2^3D_1)$ and $D_s(2^3D_3)$. The masses of $D_s(2^3D_1)$ and $D_s(2^3D_3)$ are 3383 MeV and 3469 MeV, respectively [30].

| Mode   | Channels                                                                 | Mode   | Channels                                                                 |
|--------|--------------------------------------------------------------------------|--------|--------------------------------------------------------------------------|
| $0^+ + 1^-$ | $D(2400)^0K^{*-}, D(2400)^+K^{*-}$, $D_s(2317)\phi$                     | $0^+ + 1^-$ | $D(2400)^0K^{*-}, D(2400)^+K^{*-}$, $D_s(2317)\phi$                     |
| $0^- + 1^+$ | $D^0 K_1(1270)^{-}, D^+ K_1(1270)^{0}$                                  | $0^- + 1^+$ | $D^0 K_1(1270)^{-}, D^+ K_1(1270)^{0}$                                  |
|         | $D^0 K_1(1400)^{-}, D^+ K_1(1400)^{0}$                                  |         | $D^0 K_1(1400)^{-}, D^+ K_1(1400)^{0}$                                  |
| $1^+ + 0^-$ | $D(2430)^0K^+, D(2430)^+K^{*0}$, $D_{s1}(2460)\eta, D_{s1}(2536)\eta$ | $1^+ + 0^-$ | $D(2430)^0K^+, D(2430)^+K^{*0}$, $D_{s1}(2460)\eta, D_{s1}(2536)\eta$ |
|         | $D(2420)^0K^+, D(2420)^+K^{*0}$                                         |         | $D(2420)^0K^+, D(2420)^+K^{*0}$                                         |
| $1^+ + 1^-$ | $D(2430)^0K^{*+}, D(2430)^+K^{*0}$                                     | $1^+ + 1^-$ | $D(2430)^0K^{*+}, D(2430)^+K^{*0}$                                     |
|         | $D(2420)^0K^{*+}, D(2420)^+K^{*0}$                                     |         | $D(2420)^0K^{*+}, D(2420)^+K^{*0}$                                     |
| $1^- + 1^+$ | $D^0 K_1(1270)^{-}, D^+ K_1(1270)^{0}$                                  | $1^- + 1^+$ | $D^0 K_1(1270)^{-}, D^+ K_1(1270)^{0}$                                  |
| $2^+ + 1^-$ | $D_2(2460)^0K^{*+}, D_2(2460)^+K^{*0}$                                   | $2^+ + 1^-$ | $D_2(2460)^0K^{*+}, D_2(2460)^+K^{*0}$                                   |
| $0^- + 0^-$ | $D^0 K^+, D^+ K^0, D_s\eta$                                             | $0^- + 0^-$ | $D^0 K^+, D^+ K^0, D_s\eta$                                             |
| $1^- + 0^-$ | $D^0 K^+, D^+ K^0, D_{s2}(2573)\eta$                                    | $1^- + 0^-$ | $D^0 K^+, D^+ K^0, D_{s2}(2573)\eta$                                    |
| $2^- + 0^-$ | $D_2(2460)^0K^+, D_2(2460)^+K^0$                                       | $2^- + 0^-$ | $D_2(2460)^0K^+, D_2(2460)^+K^0$                                       |
| $0^- + 2^+$ | $D^0 K_2(1430)^{-}, D^+ K_2(1430)^0$                                    | $0^- + 2^+$ | $D^0 K_2(1430)^{-}, D^+ K_2(1430)^0$                                    |

A. $D_{s1}(2700)$, $D_{s1}(2860)$ and $D_{s3}(2860)$

For kinematical reason and conservation of some quantum numbers in hadronic decay, $D_{s1}(2700)$ can only be produced through $2D D_s \rightarrow D_{s1}(2700)\eta$. The numerical results are presented in Table. 7. The first column in the table indicates three possible assignments of $D_{s1}(2700)$, where the mixture possibility is from Ref. [12] with a mixing angle $\theta = 88^\circ$. The mixing of $D_{s1}(2700)$ has also been studied in other references [9, 17, 31]. In the table, all the decay widths are very small though they are different in different assignments of $D_{s1}(2700)$.

Once $D_{s1}(2860)^-$ and $D_{s3}(2860)^-$ are assigned as the $J^P = 1^-$ and $J^P = 3^-$ members of the $1D$ family, the hadronic decay widths of $2D D_s \rightarrow D_{s1}(2860)\eta$ can also be calculated. However, predicted masses of $2D D_1$, $D_2$ and $D_2 D_s$ [30] are
close to the threshold of $D_{s1}^*(2860)/D_{s3}^*(2860)\eta$, their hadronic decays may be complicated. Therefore, we give only the results of the hadronic decay channels $D_s(2^1D_3) \rightarrow D_{s1}^*(2860)/D_{s3}^*(2860)\eta$. The decay widths for $D_s(2^1D_3) \rightarrow D_{s1}^*(2860)\eta$ MeV and $D_s(2^2D_3) \rightarrow D_{s3}^*(2860)\eta$ are 0 and 0.37 MeV, respectively.

### B. $D(2600)$ AND $D(2750)$

$D(2600)$ is possibly a $2^3S_1$, or a $1^3D_1$ $D$, or an orthogonal partner of the mixtures of $2^3S_1$ and $1^3D_1$ with $J^P = 1^-$. The hadronic decay widths of $2D D_s \rightarrow D(2600)K$ in different assignments of $D(2600)$ are given in Table. 8.

---

| Mode       | $D_s(2^1D_3)$ Channels | $D_s(2^2D_3)$ Channels |
|------------|------------------------|------------------------|
| $0^+ + 1^-$| $D(2400)^0K^{*+}, D(2400)^+K^{-0}$, $D_s(2317)\phi$ | $0^+ + 1^-$ | $D(2400)^0K^{*+}, D(2400)^+K^{-0}$, $D_s(2317)\phi$ |
| $0^- + 1^+$| $D^0K_1(1270)^+, D^+K_1(1270)^0$ | $0^- + 1^+$ | $D^0K_1(1270)^+, D^+K_1(1270)^0$ |
|           | $D^0K_1(1400)^+, D^+K_1(1400)^0$ |           | $D^0K_1(1400)^+, D^+K_1(1400)^0$ |
| $1^+ + 0^-$| $D(2430)^0K^{+}, D(2430)^+K^{-0}$, $D_s(2460)\eta, D_s(2536)\eta$ | $1^+ + 0^-$ | $D(2430)^0K^{+}, D(2430)^+K^{-0}$, $D_s(2460)\eta, D_s(2536)\eta$ |
| $1^+ + 1^-$| $D(2430)^0K^{*+}, D(2430)^+K^{-0}$ | $1^+ + 1^-$ | $D(2430)^0K^{*+}, D(2430)^+K^{-0}$ |
|           | $D^0K_1(1270)^+, D^+K_1(1270)^0$ |           | $D^0K_1(1270)^+, D^+K_1(1270)^0$ |
|           | $D^0K_1(1400)^+, D^+K_1(1400)^0$ |           | $D^0K_1(1400)^+, D^+K_1(1400)^0$ |
| $2^+ + 0^-$| $D_2(2460)^0K^{+}, D_2(2460)^+K^{-0}$ | $2^+ + 1^-$ | $D_2(2460)^0K^{+}, D_2(2460)^+K^{-0}$ |
| $0^+ + 0^-$| $D(2400)^0K^{+}, D_s(2317)\eta$ | $0^+ + 0^-$ | $D(2400)^0K^{+}, D_s(2317)\eta$ |
|           | $D(2400)^0K^0, D_s(2317)\eta, D_s(2317)\eta'$ |           | $D(2400)^0K^0, D_s(2317)\eta, D_s(2317)\eta'$ |
| $0^+ + 0^+$| $D^0K_2^+(1430)^+, D^+K_2^+(1430)^0$ | $0^- + 0^+$ | $D^0K_2^+(1430)^+, D^+K_2^+(1430)^0$ |
| $1^+ + 0^+$| $D^0K^{*+}, D^+K^{*0}, D_s\phi$ | $1^- + 0^-$ | $D^0K^{*+}, D^+K^{*0}, D_s\phi$ |
|           | $D^0K^+(1410)^+, D^+K^+(1410)^0$ |           | $D^0K^+(1410)^+, D^+K^+(1410)^0$ |
|           | $D^0K^{*+}, D^+K^{*0}, D_s\phi$ |           | $D^0K^{*+}, D^+K^{*0}, D_s\phi$ |
|           | $D^0K^+(1410)^+, D^+K^+(1410)^0$ |           | $D^0K^+(1410)^+, D^+K^+(1410)^0$ |
|           | $D^0K_2^+(1430)^+, D^+K_2^+(1430)^0$ |           | $D^0K_2^+(1430)^+, D^+K_2^+(1430)^0$ |
| $3^- + 0^-$| $(D^1D_3)^0K^{+}, (D^1D_3)^+K^{-0}, D_s(1^3D_3)\eta$ | $3^- + 0^-$ | $(D^1D_3)^0K^{+}, (D^1D_3)^+K^{-0}, D_s(1^3D_3)\eta$ |

---

**TABLE IV: OZI-allowed hadronic decay modes of $D_s(2^1D_2)$ and $D_s(2^2D_2)$.** The mass of $D_s(2^1D_2)$ and $D_s(2^2D_2)$ is 3429.5 MeV [30].
Obviously, the decay widths have large difference in different assignments of $D(2600)$, therefore the final decay widths depend heavily on the mixing angle. In the table, results corresponding to two different mixing angle are given, where the mixing angle $0.9 \leq \theta \leq 1.5$ [17] and $0.36 \leq \theta \leq 0.40$ [22].

$D(2750)$ may be a $^1D_1$ or a $^3D_3$ $D_s$ numerical results of relevant channels are given in Table. 9, where the "*' indicates an impossible channel. As indicated in Ref. [10], there are possibly two $D$ resonances close to 2750 MeV, which requires careful study of this energy region. Therefore, other possible assignments of $D(2750)$ are not studied here.

### Table V: Hadronic decay widths of $D_s(2^3D_1)$ and $D_s(2^3D_3)$ in MeV.

| Channels | Width | Channels | Width | Channels | Width | Channels | Width |
|----------|-------|----------|-------|----------|-------|----------|-------|
| $D(2400)K^{*+}$ | 13.53 | $D^{*}K^{0}$ | 0.24 | $D(2400)K^{*0}$ | 6.10 | $D^{*+}K(1430)^{*0}$ | 53.04 |
| $D(2400)+K^{*0}$ | 7.28 | $D_s\eta$ | 0.05 | $D(2400)+K^{*0}$ | 7.48 | $D^{*0}K^{+}$ | 0.00 |
| $D_s(2317)\phi$ | 2.83 | $D_s\eta$ | 1.03 | $D_s(2317)\phi$ | 2.19 | $D^{*0}K^{0}$ | 0.00 |
| $D_s(1270)+$ | 14.88 | $D(2550)K^{+}$ | 12.34 | $D^{0}K(1270)^{+}$ | 81.61 | $D_s\eta$ | 0.00 |
| $D^{*+}K(1270)^{0}$ | 14.58 | $D(2550)+K^{0}$ | 12.55 | $D^{*+}K(1270)^{+}$ | 75.06 | $D_s\eta$ | 0.16 |
| $D^{*+}K(1400)^{+}$ | 15.29 | $D^{*0}K^{+}$ | 3.91 | $D^{*0}K(1400)^{+}$ | 33.16 | $D(2550)K^{+}$ | 0.06 |
| $D_s(1400)^{0}$ | 13.32 | $D^{*+}K^{0}$ | 4.08 | $D^{*+}K(1400)^{0}$ | 36.30 | $D(2550)+K^{0}$ | 0.06 |
| $D(2430)K^{+}$ | 20.88 | $D_s\eta$ | 1.60 | $D^{0}K^{0}$ | 1.03 | $D^{*0}K^{+}$ | 0.00 |
| $D(2430)+K^{0}$ | 21.18 | $D_s\eta$ | 0.48 | $D^{*+}K^{0}$ | 0.84 | $D^{*0}K^{0}$ | 0.00 |
| $D(2420)+K^{0}$ | 13.91 | $D^{*0}K^{+}$ | 6.31 | $D(2430)K^{+}$ | 14.00 | $D_s\eta$ | 0.00 |
| $D(2420)+K^{0}$ | 14.04 | $D^{*+}K^{0}$ | 6.55 | $D(2430)+K^{0}$ | 13.98 | $D_s\eta$ | 0.95 |
| $D_s(2460)\eta$ | 4.78 | $D_s\phi$ | 2.20 | $D(2420)K^{+}$ | 1.93 | $D^{*0}K^{+}$ | 0.01 |
| $D_s(2536)\eta$ | 2.33 | $D^{*0}K^{+}$ | 20.22 | $D(2420)+K^{0}$ | 1.97 | $D^{*0}K^{+}$ | 0.01 |
| $D(2430)+K^{*0}$ | 11.41 | $D^{*+}K^{+}$ | 20.19 | $D_s(2460)\eta$ | 1.34 | $D_s\phi$ | 0.00 |
| $D(2430)+K^{0}$ | 11.26 | $D^{*+}K^{+}$ | 9.82 | $D_s(2460)\eta$ | 0.01 | $D^{*0}K^{*}(1410)^{0}$ | 38.98 |
| $D(2470)+K^{0}$ | 11.33 | $D^{*+}K^{0}$ | 9.67 | $D_s(2536)\eta$ | 0.59 | $D^{*+}K^{*}(1410)^{0}$ | 37.16 |
| $D(2420)+K^{*0}$ | 10.01 | $D^{*0}K^{+}$ | 2.76 | $D(2430)K^{*+}$ | 15.27 | $D^{*0}K^{*}(1410)^{0}$ | 68.97 |
| $D^{*0}K(1270)^{0}$ | 22.02 | $D^{*0}K^{+}(1410)^{0}$ | 0.05 | $D(2430)K^{*0}$ | 14.64 | $D^{*0}K^{*}(1410)^{0}$ | 66.56 |
| $D^{*+}K(1270)^{0}$ | 21.12 | $D^{*0}K^{+}(1410)^{0}$ | 0.04 | $D(2420)K^{*+}$ | 19.17 | $D^{*0}K^{*+}$ | 2.91 |
| $D^{*0}K(1400)^{0}$ | 10.20 | $D^{*0}K^{+}$ | 0.21 | $D(2420)K^{*0}$ | 18.90 | $D^{*+}K^{*0}$ | 2.93 |
| $D^{*+}K(1400)^{0}$ | 10.26 | $D^{*+}K^{+}$ | 0.67 | $D^{*0}K(1400)^{0}$ | 36.47 | $D^{*0}K^{*0}$ | 0.37 |
| $D^{*0}K(1400)^{0}$ | 0.23 | $D^{*+}K^{+}$ | 0.66 | $D^{*0}K(1400)^{0}$ | 36.51 | $D^{*0}K^{+}$ | 0.14 |
| $D^{*0}K(1400)^{0}$ | 4.31 | $D^{*0}K^{+}$ | 0.14 |
| $D^{*+}K(1400)^{0}$ | 3.87 | $D^{*0}K^{+}$ | 0.01 |
| $D^{*+}K(1400)^{0}$ | 25.44 | $D^{*0}K^{+}$ | 0.61 |
| $D^{*+}K(1400)^{0}$ | 25.54 | $D^{*0}K^{+}$ | 0.62 |
| $D^{*0}K(1400)^{0}$ | 61.94 | $D^{*0}K^{+}$ | 0.00 |

### IV. Conclusions and Discussions

In this work, the hadronic decay properties of the highly excited $2^D D_s$ resonances are studied in $^3P_0$ model. The hadronic decay widths of all possible OZI-allowed channels of the highly excited $2^D D_s$ resonances have been calculated. The dominant decay modes of $D_s(2^3D_1)$ are $D(2430)K$, $D^{*+}K(1270)$ and $DK^{*}(1410)$ et al, while the dominant decay modes of $D_s(2^3D_3)$ are $D(1430)$ and $D^{*+}K(1410)$ et al. The dominant decay modes of $D_s(2^1D_2)$ are $D^{*+}K$, $D^{*+}K(1270)$ and $DK^{*}(1410)$ et al, while the dominant decay modes of $D_s(2^1D_3)$ are $DK^{*}(1410)$ and $D^{*+}K$ et al. The $2^D D_s$ resonances are suggested to
D* resonances. Possible hadronic decay channels are 2D S1 states. The threshold of D* D* (2860) is from Ref. [12].

| State                  | 2D S1 → D* D* (2700)η | 2D D* → D* D* (2700)η | 2D D* → D* D* (2700)η | 2D D* → D* D* (2700)η |
|------------------------|------------------------|------------------------|------------------------|------------------------|
| D* D* (2700) (2S 1)    | 2.48                   | 1.43                   | 3.98                   | 6.26                   |
| D* D* (2700) (1D 1)    | 0.78                   | 0.03                   | 8.39                   | 3.19                   |
| D* D* (2700) (mixture) | 0.87                   | 0.02                   | 8.08                   | 3.50                   |

be observed in these dominant hadronic decay channels in forthcoming experiments.

D* D* (2700), D* D* (2860) and D* D* (2860) can be produced from the hadronic decays of the highly excited 2D D* states. Possible hadronic decay channels are 2D D* → D* D* (2700)η and 2D D* → D* D* (2860)/D* D* (2860)η, respectively. In every possible assignments of D* D* (2700), all the hadronic decay widths are very small. The hadronic decay widths of D* D* (2860) → D* D* (2700)η and D* D* (2860) → D* D* (2700)η are also very small. It is not suitable to classify these resonances according to their hadronic production from the 2D D* states. The threshold of
TABLE VIII: Hadronic decay widths (in MeV) of $2D_s \to D(2600)K$ in different assignments of $D(2600)$.

| Assignment\Mode | $2^3D_1 \to D(2600)^+K^0$ | $2^3D_3 \to D(2600)^+K^0$ | $2^1D_2 \to D(2600)^+K^0$ | $2^3D_2 \to D(2600)^+K^0$ |
|-----------------|-----------------------------|-----------------------------|----------------------------|-----------------------------|
| $D(2600)^+(2^3S_1)$ | 9.85                        | 22.27                       | 28.80                      | 26.35                      |
| $D(2600)^+(1^3D_1)$ | 36.20                       | 0.87                        | 138.02                     | 52.26                      |
| $D(2600)^+(\text{mixture}[17])$ | 37.99 − 45.33               | 0.00 − 4.86                 | 90.81 − 136.75             | 40.85 − 51.93              |
| $D(2600)^+(\text{mixture}[25])$ | 25.53 − 27.14               | 15.87 − 16.63               | 39.22 − 41.67              | 28.68 − 29.25              |

| Assignment\Mode | $2^3D_1 \to D(2600)^0K^+$ | $2^3D_3 \to D(2600)^0K^+$ | $2^1D_3 \to D(2600)^0K^+$ | $2^3D_3 \to D(2600)^0K^+$ |
|-----------------|-----------------------------|-----------------------------|----------------------------|-----------------------------|
| $D(2600)^0(2^3S_1)$ | 8.89                        | 22.96                       | 29.10                      | 25.76                      |
| $D(2600)^0(1^3D_1)$ | 42.35                       | 0.82                        | 145.99                     | 56.35                      |
| $D(2600)^0(\text{mixture}[17])$ | 44.92 − 51.24               | 0.00 − 5.15                 | 99.58 − 145.22             | 38.37 − 53.97              |
| $D(2600)^0(\text{mixture}[25])$ | 26.03 − 27.88               | 16.50 − 17.27               | 43.07 − 45.91              | 25.45 − 25.92              |

TABLE IX: Hadronic decay widths (in MeV) of $2D_s \to D(2750)K$ in different assignments of $D(2750)$.

| Assignment\Mode | $2^3D_1 \to D(2750)^+K^0$ | $2^3D_3 \to D(2750)^+K^0$ | $2^1D_2 \to D(2750)^+K^0$ | $2^3D_2 \to D(2750)^+K^0$ |
|-----------------|-----------------------------|-----------------------------|----------------------------|-----------------------------|
| $D(2750)^+(1^3D_3)$ | −                           | 6.02                        | 45.59                      | 52.32                      |
| $D(2750)^+(1^3D_1)$ | 1.91                        | 0.44                        | 48.27                      | 20.64                      |

| Assignment\Mode | $2^3D_1 \to D(2750)^0K^+$ | $2^3D_3 \to D(2750)^0K^+$ | $2^1D_3 \to D(2750)^0K^+$ | $2^3D_3 \to D(2750)^0K^+$ |
|-----------------|-----------------------------|-----------------------------|----------------------------|-----------------------------|
| $D(2750)^0(1^3D_3)$ | −                           | 5.81                        | 49.98                      | 56.97                      |
| $D(2750)^0(1^3D_1)$ | 2.58                        | 0.49                        | 53.22                      | 22.28                      |

$D_{s1}^{*}(2860)/D_{s3}^{*}(2860)\eta$ are close to the theoretical predicted masses of $2D_1$, $3D_2$ and $1D_2$, and relevant hadronic decays may be complicated.

Hadronic decay widths of $2D_s \to D(2600)K$ and $2D_s \to D(2750)K$ in different assignments of $D(2600)$ and $D(2750)$ have also been calculated. The hadronic decay widths may be large, and the numerical results are different in different assignments of $D(2600)$ and $D(2750)$. If the $2D_s$ resonances are observed in forthcoming experiments, the measure of these hadronic decay widths will help us to understand $D(2600)$ and $D(2750)$.

In our paper, the uncertainties of the input parameters and the model have not been studied. The detail of possible mixing of some resonances has neither been explored. More theoretical study of these highly excited resonances are required. Of course, the most important thing is to expect more highly excited $D_s$ resonances observed in forthcoming experiments.

Acknowledgments

This work is supported by National Natural Science Foundation of China under the grants: 11075102 and 11475111. It is also supported by the Innovation Program of Shanghai Municipal Education Commission under the grant No. 13ZZ066.

[1] K. Abe, et al. (Belle Collaboration), hep-ex/0608031.
[2] B. Aubert, et al. (BaBar Collaboration), Phys. Rev. D 80, 092003 (2009).
[3] K.A. Olive, et al. (Particle Data Group), Chin. Phys. C38, 090001 (2014).
[4] R. Aaij et al. (LHCb Collaboration), Phys. Rev. Lett. 113, 162001 (2014).
[5] R. Aaij et al. (LHCb Collaboration), Phys. Rev. D 90, 072003 (2014).
[6] P. del Amo Sanchez et al. (BaBar Collaboration), Phys. Rev. D 82, 111101 (2010).
[7] F.E. Close, C.E. Thomas, O. Lakhina and E.S. Swanson, Phys. Lett. B 647, 159 (2007).
[8] P. Colangelo, F.De Fazio, S. Nicoti and M. Rizzi, Phys. Rev. D 77, 014012 (2008).
[9] Bing Chen, Deng-Xia Wang and Ailin Zhang, Phys. Rev.
[10] Bing Chen, Ling Yuan and Ailin Zhang, Phys. Rev. D 83, 114025 (2011).
[11] Bo Zhang, Xiang Liu, Wei-Zhen Deng and Shi-Lin Zhu, Eur. Phys. J. C 50, 617 (2007).
[12] Stephen Godfrey and Ian T. Jardine, Phys. Rev. D 89, 074023 (2014).
[13] Ailin Zhang, Nucl. Phys. A 856, 88 (2011).
[14] E.V. Beveren and G.Rupp, Phys. Rev. Lett 97, 202001 (2006).
[15] P. Colangelo, F. De Fazio and S. Nicotri, Phys.Lett. B 642, 48 (2006).
[16] Xian-Hui Zhong and Qiang Zhao, Phys.Rev. D 78, 014029 (2008).
[17] De-Min Li, Peng-Fei Ji and Bing Ma, Eur. Phys. J. C 71, 1528 (2011).
[18] Zhi-Feng Sun, Jie-Sheng Yu, Xiang Liu and Takayuki Matsuki, Phys. Rev. D 82, 111501 (R) (2010).
[19] Xian-Hui Zhong, Phys. Rev. D 82, 114014 (2010).
[20] P. Colangelo, F. De Fazio, F. Giannuzzi and S. Nicotri, Phys. Rev. D 86, 054024 (2012).
[21] L. Micu, Nucl. Phys. B 10, 521 (1969).
[22] A. Le Yaouanc, L. Oliver, O. Pène and J.C. Raynal, Phys. Rev. D 8, 2223 (1973); 9, 1415 (1974); 11, 1272 (1975).
[23] A. Le Yaouanc, L. Oliver, O. Pène and J.C. Raynal, Phys. Lett. B 71, 57 (1977); 71, 397 (1977); 72, 57 (1977).
[24] A. Le Yaouanc, L. Oliver, O. Pène and J.C. Raynal, Hadron Transitions in the Quark Model, Gordon and Breach Science Publishers, New York, 1987.
[25] Zhi-Gang Luo, Xiao-Lin Chen and Xiang Liu, Phys. Rev. D 79, 074020 (2009).
[26] Li-Jin Chen, Dan-Dan Ye and Ailin Zhang, Eur. Phys. J. C 74, 3031 (2014).
[27] M. Jacob and G.C. Wick, Ann. Phys. (N. Y.) 7, 404 (1959); 281, 774 (2000).
[28] S. Godfrey and N. Isgur, Phys. Rev. D 32, 189 (1985).
[29] Zhi-Feng Sun and Xiang Liu, Phys. Rev. D 80, 074037 (2009).
[30] D. Ebert, R.N. Faustov and V.O. Galkin, Eur. Phys. J. C 66, 197 (2010).
[31] Ling Yuan, Bing Chen and Ailin Zhang, arXiv:123.0370.