A measurement of the relative branching fraction of $B_s^0 \to J/\psi f_0(980), f_0(980) \to \pi^+\pi^-$ to $B_s^0 \to J/\psi \phi, \phi \to K^+K^-$ is presented. The decay mode $B_s^0 \to J/\psi f_0(980)$ is an interesting mode since it is a CP eigenstate and allows the measurement of the CP-violating phase $\phi_s$. Using approximately 8 fb$^{-1}$ of data recorded with the DØ detector at the Fermilab Tevatron Collider, a relative branching fraction of $0.210 \pm 0.032 \text{ (stat)} \pm 0.036 \text{ (syst)}$ is found.

Preliminary Result
I. INTRODUCTION

Current measurements of the CP-violating phase in $B^0_s$ mixing, $\phi_s$, [1, 2], using $B^0_s \to J/\psi \phi$ decays have absolute values that are larger than predicted by the Standard Model (SM) [3]. However, the deviation from the SM is not yet statistically significant due to the magnitude of the uncertainty in the measured value of $\phi_s$. Measuring $\phi_s$ using an additional decay mode can aid in reducing this uncertainty. The decay products in $B^0_s \to J/\psi f_0(980)$ are in a CP eigenstate and can provide a more direct measurement of $\phi_s$ compared to $B^0_s \to J/\psi \phi$. Due to a lower expected branching fraction, it is expected that this mode will not provide as precise a measurement of $\phi_s$ as found from $B^0_s \to J/\psi \phi$ decays; however, the systematics will be different and so it will provide a complementary and important cross check of the $B^0_s \to J/\psi \phi$ result.

Based on estimates the relative branching fraction should be large. Using hadronic $D^+_s$ decays, Stone and Zhang [4, 5] estimated the relative width to be:

$$ R \equiv \frac{\Gamma(B^0_s \to J/\psi f_0(980); f_0(980) \to \pi^+\pi^-)}{\Gamma(B^0_s \to J/\psi \phi; \phi \to K^+K^-)} \approx 0.20. \tag{1} $$

A second estimate comes from a CLEO measurement [6] using the decays $D^+_s \to f_0 e^+\nu$ and $D^+_s \to \phi e^+\nu$ giving $R = (0.42 \pm 0.11)$. The Belle collaboration has searched for $B^0_s \to J/\psi f_0(980)$ [7, 8], and reports an upper limit at the 90\% CL of $R < 0.275$. Recently the LHCb collaboration has reported [9] a first measurement of $R = 0.252^{+0.046+0.027}_{-0.032-0.033}$

The Belle collaboration has also released a new measurement of the branching fraction $B(B^0_s \to J/\psi f_0(980); f_0(980) \to \pi^+\pi^-) = (1.16^{+0.31}_{-0.19} \text{(stat.)}^{+0.15}_{-0.17} \text{(syst.)}^{+0.26}_{-0.18} \text{(N}B^0_s/B^0_s^{*})) \times 10^{-5}$ [10].

This note provides a new measurement of the relative branching fraction from DØ.

II. RELATIVE BRANCHING FRACTION

To determine an absolute branching fraction ($B$), various efficiencies, branching fractions, and cross sections need to be known, as well as the integrated luminosity. However, by measuring a relative branching fraction, several terms common to both the $B^0_s \to J/\psi f_0(980)$ branching fraction and the $B^0_s \to J/\psi \phi$ branching fraction cancel giving:

$$ R = \frac{B(B^0_s \to J/\psi f_0(980); f_0(980) \to \pi^+\pi^-)}{B(B^0_s \to J/\psi \phi; \phi \to K^+K^-)} = \frac{N_{B^0_s \to J/\psi f_0(980)} \times \varepsilon_{reco}^{B^0_s \to J/\psi \phi}}{N_{B^0_s \to J/\psi \phi} \times \varepsilon_{reco}^{B^0_s \to J/\psi f_0(980)}}. \tag{2} $$

All that is required to measure a relative branching fraction are the relative yields and the relative reconstruction efficiencies of the two decay modes, $\varepsilon_{reco}^{B^0_s \to J/\psi \phi}$ and $\varepsilon_{reco}^{B^0_s \to J/\psi f_0(980)}$.

III. SELECTION CUTS

A. Analysis Cuts

The data set of an integrated luminosity of approximately 8 fb$^{-1}$ was divided into four periods corresponding to different detector configurations called RunIIa, RunIIb1, RunIIb2 and RunIIb3. The event selection cuts are based on an older $J/\psi \phi$ analysis [11].

The data sample consisted of events that satisfied either a muon or a dimuon trigger. The initial sample of $B^0_s \to J/\psi f_0(980)$ was found by first reconstructing $J/\psi \to \mu^+\mu^-$ candidates by requiring that two oppositely charged muon candidates with transverse momentum $p_T > 1.5$ GeV form a common vertex, see Fig. 1. Since DØ has a limited ability to separate kaons from pions, all reconstructed tracks are considered in this analysis. The tracks are assigned the pion mass when searching for $B^0_s \to J/\psi f_0(980)$ and the kaon mass when searching for $B^0_s \to J/\psi \phi$. Two tracks with a minimum $p_T$ of 300 MeV, having an invariant mass 0.7 GeV $< M_{\pi^+\pi^-} < 1.2$ GeV, and being consistent with coming from a common vertex were considered as $f_0(980)$ candidates. Finally, the $\mu^+\mu^-\pi^+\pi^-$ candidates were required to have a common vertex and have an invariant mass between 5.0–5.8 GeV.

Similar requirements were applied to the initial sample of $B^0_s \to J/\psi \phi$ candidates. The only different requirements were that 0.91 GeV $< M_{K^+K^-} < 1.05$ GeV and the $\mu^+\mu^- K^+K^-$ candidates were required to have an invariant mass between 5.0–5.8 GeV. Due to the invariant mass requirements on $M_{\pi^+\pi^-}$ and $M_{K^+K^-}$, two tracks cannot be
FIG. 1: The $\mu^+\mu^-$ invariant mass distribution for a small subset of the data.

considered both a $f_0(980)$ and a $\phi$ candidate. The final data sample was then formed by applying the additional requirements:

- All runs without optimal performance of muon, silicon microstrip and central fiber trackers are omitted.
- All events that only fired a trigger that required muons with a large impact parameter were removed.

$J/\psi$ selection:

- Both muons are required to be detected as a track segment in either one or three layers of the muon system and be matched to a central track.
- At least one muon must be detected as a track segment in three layers of the muon system.
- Both muons must have at least one hit in the silicon microstrip tracker.
- $2.9 \text{ GeV} < M_{\mu^+\mu^-} < 3.2 \text{ GeV}$

$f_0(980)$ ($\phi$) selection:

- Both pions (kaons) from the $f_0(980)$ ($\phi$) candidate must have at least 2 hits in the central fiber tracker.
- Both pions (kaons) from the $f_0(980)$ ($\phi$) candidate must have at least 2 hits in the silicon microstrip tracker.
- Both pions (kaons) from the $f_0(980)$ ($\phi$) candidate must have at least 8 hits total in the silicon microstrip tracker and the central fiber tracker.
- The momentum of the leading pion (kaon) from the $f_0(980)$ ($\phi$) candidate must be greater than 1.4 GeV.
- $f_0(980)$ ($\phi$) candidate $p_T$ must be greater than 1.6 GeV.
FIG. 2: BDT distribution after training for both signal (blue) and inclusive background (red).

$B^0_\mathrm{s}$ selection:

- $0.91 \text{ GeV} < M_{\pi^+\pi^-} < 1.05 \text{ GeV}$ (when searching for $J/\psi f_0(980)$.)
- $1.01 \text{ GeV} < M_{K^+K^-} < 1.03 \text{ GeV}$ (when searching for $J/\psi \phi$.)
- $p_T(B^0_\mathrm{s}) > 5.0 \text{ GeV}$
- Proper decay length [12], $L$, significance, $L/\sigma(L) > 5$, where $\sigma(L)$ is the uncertainty on the proper decay length.

B. Boosted Decision Trees

It is known that boosted decision trees (BDT) [13, 14] are a powerful tool for separating signal from background. Signal and background samples are used to train the BDT and a discriminant is determined for each event. By making a selection on the value of the BDT discriminant, the signal to background ratio can be vastly improved. We use the Monte Carlo (MC) PYTHIA program [15] to generate $B^0_\mathrm{s}$ and the EVTGEN program [16] to simulate its decay. Two MC background samples were produced: a prompt sample (directly produced $J/\psi$) and an inclusive sample (all decay processes $B^0_\mathrm{s} \rightarrow J/\psi + X$). A MC signal sample of $B^0_\mathrm{s} \rightarrow J/\psi f_0(980)$ events was then used to train the BDT on both the prompt and inclusive background. A BDT discriminant was found for both the prompt (BDT pro) and inclusive sample (BDT inc) and used in the analysis. A total of 36 different kinematic variables (see Appendix A) were used to train the BDT consisting of isolation variables, transverse momentum of the daughters and grand-daughters of the $B^0_\mathrm{s}$ and vertex quality of the $B^0_\mathrm{s}$ and its daughters. Figures 2 and 3 show the BDT distributions for the training and test samples for the inclusive and prompt background.

The BDT cuts were determined only using the 1 fb$^{-1}$ of RunIIa data. A narrow window around the nominal $f_0(980)$ mass was chosen to keep the signal to noise ratio high. Using a mass cut of 0.96–1.0 GeV on the $\pi^+\pi^-$ mass, the BDT cut value was chosen where both $S/\sqrt{B}$ and the signal yield were high. In this way, the BDT discriminant for both the inclusive and prompt BDT was required to be greater than 0.35.
A clear $B_{s}^{0}$ peak is found when the $\pi^{+}\pi^{-}$ invariant mass is near the nominal $f_{0}(980)$ mass. It is expected that the $B_{s}^{0}$ signal can be fitted to a Gaussian distribution, which provides a fitted mean mass ($\mu$) and width ($\sigma$) for the $B_{s}^{0}$ peak. Since backgrounds are large, a cut of $\pm 2\sigma$ around the fitted $B_{s}^{0}$ peak is used to identify the $f_{0}(980)$ mass peak. A clear $f_{0}(980)$ mass peak is observed when the $\mu^{+}\mu^{-}\pi^{+}\pi^{-}$ invariant mass is within $\pm 2\sigma$ of the fitted $B_{s}^{0}$ mass, see Fig. 4. To decide on a $\pi^{+}\pi^{-}$ mass window to use for this analysis, a fit to the $f_{0}(980)$ mass peak is performed. The $f_{0}(980)$ has a large width [17] and is just under the $KK$ mass threshold. This changes the line shape from a simple Breit Wigner form, particularly for higher masses and so the $\pi^{+}\pi^{-}$ mass distribution is fitted using a functional form based on Flatté [18], convoluted with a Gaussian function, that takes into account the opening of the $KK$ threshold. The lineshape found from fitting the $f_{0}(980)$ in MC is used to fit the data, see Fig. 5. A $\pi^{+}\pi^{-}$ invariant mass cut of 0.91–1.05 GeV is applied to identify $B_{s}^{0}\rightarrow J/\psi f_{0}(980)$ and is shown in Fig. 6. The $B_{s}^{0}\rightarrow J/\psi f_{0}(980)$ mass distribution was fit to a Gaussian signal with a background function consisting of a second-degree polynomial and a Gaussian function at lower invariant mass to take into account partially reconstructed $B$ decays.

Using identical cuts (except for the cut on the $\phi$ mass, see Fig. 7), a clear $J/\psi\phi$ peak is found and is shown in Fig. 8. Since the $\phi$ peak is so narrow, the backgrounds are much smaller for $B_{s}^{0}\rightarrow J/\psi\phi$.

An unbinned likelihood fit was used to determine the candidate yields in each sample. It was found that the results from the likelihood fit were nearly independent of the initial fit parameter starting values, i.e., the yield changed by only 2-3 events when the initial fit parameters were varied. The fit to the $J/\psi f_{0}(980)$ mass distribution shown in Fig. 6 gives the following results (statistical uncertainties only):

$$B_{s}^{0} \text{ mass} = 5.3747 \pm 0.0036 \text{ GeV}; \quad \sigma = 0.0290 \pm 0.0044 \text{ GeV}; \quad 498 \pm 74 \ B_{s}^{0} \rightarrow J/\psi f_{0}(980) \text{ candidates.}$$

The $\mu^{+}\mu^{-}K^{+}K^{-}$ mass distribution was fit for a $B_{s}^{0}\rightarrow J/\psi\phi$ signal using a double Gaussian function with a second-order polynomial background. A fit to the $J/\psi\phi$ distribution shown in Fig. 8 gives the following results (statistical uncertainties only):

$$B_{s}^{0} \text{ mass} = 5.3631 \pm 0.0008 \text{ GeV}; \quad 2863 \pm 61 \ B_{s}^{0} \rightarrow J/\psi\phi \text{ candidates.}$$

From the above fits, we find the relative yield of $B_{s}^{0}\rightarrow J/\psi f_{0}(980)$ to $B_{s}^{0}\rightarrow J/\psi\phi$ to be $0.174 \pm 0.026$ (stat). The relative yields must now be corrected by the relative efficiencies in order to determine $R$. 

IV. YIELD RESULTS

FIG. 3: BDT distribution after training for both signal (blue) and prompt background (red).
FIG. 4: $\pi^+\pi^-$ invariant mass distribution peaking at the $f_0(980)$ mass when the $J/\psi\pi^+\pi^-$ mass is $\pm 2\sigma$ around the fitted $B_s^0$ mass.

FIG. 5: $\pi^+\pi^-$ invariant mass distribution from $B_s^0 \to J/\psi f_0(980)$ MC fitted to functional form based on Flatté which takes into account the opening of the $KK$ threshold.

V. EFFICIENCIES

To determine the efficiencies of the analysis, MC signal samples were used. To take into account the effects of the instantaneous luminosity, the MC samples were overlayed with zero bias data collected during each run period. In the generation of both the $J/\psi\phi$ and the $J/\psi f_0(980)$ signal MC’s, a preselection requirement of $p_T > 0.4$ GeV was demanded on both kaons (pions) from the $\phi(f_0(980))$. Since the $p_T$ distributions for the pions and kaons may be different, the preselection efficiencies of this cut must be determined. To determine the preselection cut efficiencies, two additional MC sets were also generated with no $p_T$ cuts on the pions (kaons). By comparing these two results, the preselection cut efficiencies were determined.

Approximately 10,000 MC events were needed to determine the preselection efficiencies to approximately 0.01. The final overall preselection efficiency for $J/\psi\phi$ was determined to be 0.795 $\pm$ 0.011 and for $J/\psi f_0(980)$ was 0.594 $\pm$ 0.0093.

We found that the reconstruction efficiencies depended heavily on the MC sample used since the instantaneous luminosity was different for the various run periods, which affected the efficiency for reconstructing tracks. Therefore we determined the reconstruction efficiencies for each run range separately. The instantaneous luminosities for runs taken during RunIIb3 were similar to the instantaneous luminosities for runs taken during RunIIb2 so the recon-
**FIG. 6:** $\mu^+\mu^-\pi^+\pi^-$ mass distribution peaking at the $B_0^s$ mass when the $\pi^+\pi^-$ mass is between 0.91 and 1.05 GeV.

**FIG. 7:** $K^+K^-$ invariant mass distribution peaking at the $\phi$ mass when the $\mu^+\mu^-K^+K^-$ mass is $\pm 2\sigma$ around the fitted $B_0^s$ mass.
FIG. 8: $\mu^+\mu^- K^+ K^-$ mass distribution peaking at the $B^0_s$ mass from 8 fb$^{-1}$ of data.

TABLE I: The total reconstruction efficiency for $B^0_s \to J/\psi \phi$ and $B^0_s \to J/\psi f_0(980)$ for various running periods. The total reconstruction efficiency is a product of the preselection efficiency and the reconstruction efficiency.

| Sample | total reconstruction efficiency |
|--------|-------------------------------|
| $B^0_s \to J/\psi \phi$ RunIIa | $0.0231 \pm 0.0004$ |
| $B^0_s \to J/\psi \phi$ RunIIb1 | $0.0191 \pm 0.0004$ |
| $B^0_s \to J/\psi \phi$ RunIIb2 | $0.00636 \pm 0.00018$ |
| $B^0_s \to J/\psi f_0(980)$ RunIIa | $0.0191 \pm 0.0004$ |
| $B^0_s \to J/\psi f_0(980)$ RunIIb1 | $0.0146 \pm 0.0003$ |
| $B^0_s \to J/\psi f_0(980)$ RunIIb2 | $0.00529 \pm 0.00015$ |

The reconstruction efficiencies should be similar for RunIIb2 and RunIIb3. Table I shows the results on the efficiency analysis using MC signal samples. Table I shows that the absolute reconstruction efficiencies vary in each run period, however Table II show that the relative reconstruction efficiencies are relatively stable. However, the differences in relative reconstruction efficiency is considered a systematic uncertainty on $R$.

TABLE II: Reconstruction efficiencies for different run periods.

| Run period | Relative reconstruction efficiency $\frac{\varepsilon_{B^0_s \to J/\psi f_0(980)}}{\varepsilon_{B^0_s \to J/\psi \phi}}$ |
|------------|--------------------------------------------------|
| RunIIa     | $1.21 \pm 0.03$                                 |
| RunIIb1    | $1.31 \pm 0.04$                                 |
| RunIIb2    | $1.20 \pm 0.05$                                 |
VI. RATIO OF BRANCHING FRACTIONS

Using the relative yields and the relative efficiencies shown above we find for the ratio of branching fractions:

\[
R = \frac{N_{B^0_s \rightarrow J/\psi f_0(980)} \times \frac{B_{s,\text{non-resonant}}}{\varepsilon_{\text{p reco}}}}{N_{B^0_s \rightarrow J/\psi f_0(980)} \times \varepsilon_{\text{p reco}}} = 0.210 \pm 0.032 \text{ (stat)}
\]

VII. SYSTEMATIC UNCERTAINTY STUDIES

A. \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) background studies

One possible peaking background that would affect the \(B^0_s \rightarrow J/\psi f_0(980)\) yield measurement is the non-resonant \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) background. This background was studied by measuring the \(B^0_s\) yields in \(\pi^+\pi^-\) invariant mass less than the \(f_0(980)\) mass. The \(\pi^+\pi^-\) mass distribution from \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) background where the \(\pi^+\pi^-\) are non-resonant should have a much broader distribution, so determining the \(B^0_s\) yield for lower \(\pi^+\pi^-\) masses will allow a determination of the contamination in the \(f_0(980)\) signal region.

In determining the \(\pi^+\pi^-\) mass window to study, it is important to choose a window where one does not expect other resonances (i.e., \(B^0_s \rightarrow J/\psi K^*\)). The \(\pi^+\pi^-\) mass window of 0.8–0.9 GeV was chosen since in this mass range there should not be any \(B^0_s \rightarrow J/\psi K^*\) events. As can be seen from Table III the number of Monte Carlo \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) events in the \(\pi^+\pi^-\) mass region 0.80–0.90 GeV is approximately 65% of those found in the \(\pi^+\pi^-\) signal region of 0.91–1.05 GeV. By determining the \(B^0_s\) yield in the \(\pi^+\pi^-\) mass region 0.80–0.90 GeV in data, the expected \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) non-resonant background in the signal region can be determined by simple scaling.

Figure 9 shows the \(B^0_s\) mass distribution in data for the \(\pi^+\pi^-\) mass region 0.8–0.9 GeV. In fitting the distribution for any possible signal, the signal \(\mu\) and \(\sigma\) are constrained to be the values found from the fit to the \(B^0_s\) mass in the \(f_0(980)\) signal region. The fit yields 80 ± 75 events, giving no statistically significant evidence of any \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) non-resonant background.

Because there are large backgrounds in the lower \(\pi^+\pi^-\) mass regions, it is difficult to determine a small \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) non-resonant background. By applying additional cuts on the trailing pion \(p_T < 1\) GeV and the trailing muon \(p_T > 3.5\) GeV, the backgrounds can be reduced. Figure 10 shows the \(\mu^+\mu^-\pi^+\pi^-\) mass distribution for \(\pi^+\pi^-\) mass within the signal region of 0.91–1.05 GeV with the additional cuts on the trailing pion \(p_T < 1\) GeV and the trailing muon \(p_T > 3.5\) GeV. A \(B^0_s\) peak is still present in the data, but with much reduced low \(\pi^+\pi^-\) mass backgrounds. Figure 11 shows the \(\mu^+\mu^-\pi^+\pi^-\) mass distribution for \(\pi^+\pi^-\) mass within the sideband region of 0.8–0.9 GeV with the additional cuts on the trailing pion \(p_T < 1\) GeV and the trailing muon \(p_T > 3.5\) GeV. No evidence of any \(B^0_s\) peak is seen, again showing there is no evidence of any statistically significant \(B^0_s \rightarrow J/\psi \pi^+\pi^-\) non-resonant background in the data. The \(M_{\pi^+\pi^-}\) mass cut removes any possible background from \(B^0_s \rightarrow J/\psi \phi\) and \(B^0_s \rightarrow J/\psi K^*\).

B. Analysis cut variation

To cross check that the results do not vary with the exact value of the analysis cuts, the choice for each analysis cut was varied around its nominal value. This is an important test since the selection criteria was determined with 1 fb\(^{-1}\) data from RunIIa, and it is important to verify that this did not introduce a bias into the measurement. Table IV shows the results from this study. As can been seen from the table, the value of \(R\) does not depend significantly on the exact choice of selection requirement.
FIG. 9: $\mu^+\mu^-\pi^+\pi^-$ mass distribution for a $\pi^+\pi^-$ mass range of 0.8–0.9 GeV.

TABLE IV: Fractional change due to varying the exact choice of analysis cuts on the relative branching fraction

| Cut                      | $\varepsilon (J/\psi)$ | $\varepsilon (J/\psi f_0)$ | event yield $B_s^0 \rightarrow J/\psi f_0$ | event yield $B_s^0 \rightarrow J/\psi f_0$ | effect on $R$ |
|--------------------------|-------------------------|----------------------------|--------------------------------|--------------------------------|---------------|
| BDT inc $>$ 0.3          | 1.000                   | 1.017                      | 1.020                          | 0.958                          | 0.96          |
| BDT inc $>$ 0.4          | 0.993                   | 0.980                      | 0.975                          | 0.945                          | 0.98          |
| BDT pro $>$ 0.3          | 1.000                   | 1.002                      | 1.000                          | 1.007                          | 1.01          |
| BDT pro $>$ 0.4          | 1.002                   | 1.000                      | 1.000                          | 0.991                          | 0.99          |
| $p_T(B^0_s)$ $>$ 4.5 GeV | 0.997                   | 1.000                      | 1.000                          | 1.000                          | 0.99          |
| $p_T(B^0_s)$ $>$ 5.5 GeV | 1.000                   | 0.995                      | 1.000                          | 0.952                          | 0.95          |
| $p_T(f_0(980))$ $>$ 1.0 GeV | 1.000               | 1.000                      | 1.000                          | 1.000                          | 1.00          |
| $p_T(f_0(980))$ $>$ 2.0 GeV | 1.000               | 0.987                      | 1.000                          | 0.980                          | 0.99          |
| $\pi/K$ $p_T$ $>$ 1.0 GeV | 1.210                   | 1.099                      | 1.172                          | 1.133                          | 1.06          |
| $\pi/K$ $p_T$ $>$ 1.8 GeV | 0.724                   | 0.771                      | 0.797                          | 0.744                          | 0.88          |
| $L/\sigma(L)$ $>$ 4     | 1.057                   | 1.047                      | 1.056                          | 1.035                          | 1.01          |
| $L/\sigma(L)$ $>$ 6     | 0.946                   | 0.951                      | 0.944                          | 0.967                          | 1.02          |

C. Fitting cross checks

Due to large backgrounds arising from combinatorics and partially reconstructed $B$ decays, there are significant uncertainties in the exact background shape. Therefore different parameterizations were used to describe the background and different fit regions were used to fit the data. The background polynomial was changed from a second-degree polynomial to a third-degree polynomial. The fit range was changed from the nominal 5.1–5.8 GeV and finally a different functional form for the background was used by changing the background shape to a polynomial plus an exponential.

As can be seen from Table V, there is a fairly large variation in the number of signal events for $B^0_s \rightarrow J/\psi f_0(980)$,
FIG. 10: $\mu^+\mu^-\pi^+\pi^-$ mass distribution for a $\pi^+\pi^-$ mass range 0.91–1.05 GeV with the additional requirements that the trailing pion $p_T < 1$ GeV and the trailing muon $p_T > 3.5$ GeV.

FIG. 11: $\mu^+\mu^-\pi^+\pi^-$ mass distribution for a $\pi^+\pi^-$ mass range 0.8–0.9 GeV with the additional requirements that the trailing pion $p_T < 1$ GeV and the trailing muon $p_T > 3.5$ GeV.
indicating that the background shape is difficult to model. This fitting systematic gives the largest systematic uncertainty on $R$. A study was performed using same-sign pions and forming the mass distribution from $\mu^+\mu^-\pi^\pm\pi^\mp$. However, it was found the the same sign pion distribution did not describe the measured background and so could not be used to help constrain the background shape, see Fig. 12. A similar study of varying the fitting choices was performed on the $B_0^s \rightarrow J/\psi\phi$ sample, however since the backgrounds are much smaller and easier to describe the event yield numbers changed by less than 1%.

The presence of $B^0 \rightarrow J/\psi\pi^+\pi^-$ was checked by including this channel in the fit. A fit consistent with zero events was found, although forcing a number of $B^0$ events while still maintaining an acceptable fit resulted in a variation of yield within the indicated systematic uncertainty.

A summary of the uncertainties on the BR are summarized in Table VI.

### TABLE V: Effects of changing the fitting choices

| Parameter                                                                 | $B_0^s \rightarrow J/\psi f_0(980)$ yield |
|---------------------------------------------------------------------------|-------------------------------------------|
| Nominal fit (Gaussian signal + second order polynomial background with fit range 5.1–5.8 GeV) | 498 ± 74                                  |
| Third degree polynomial background                                         | 446 ± 72                                  |
| Background function exponential+polynomial                                 | 423 ± 67                                  |
| Fit range 5.1–5.6 GeV                                                     | 437 ± 78                                  |
| Fit range 5.15–5.8 GeV                                                    | 427 ± 63                                  |
| Fit range 5.05–5.8 GeV                                                    | 449 ± 71                                  |

### FIG. 12: $\mu^+\mu^-\pi\pi$ mass distribution for a $\pi\pi$ mass range 0.91–1.05 GeV. The black circles correspond to oppositely charged pions and the red squares correspond to like sign pions. The data is a subset of the full 8 fb$^{-1}$ sample, consisting of only RunIIa and RunIIb2 data.

A summary of the uncertainties on the BR are summarized in Table VI.

### TABLE VI: Statistical and systematic uncertainties in branching fraction ratio, $R$

| Source                                      | Uncertainty |
|---------------------------------------------|-------------|
| Statistical                                 | 0.149       |
| Systematic from fitting                     | 0.150       |
| Systematic from different MC samples        | 0.0858      |
VIII. FINAL BRANCHING FRACTION RATIO

The decay $B_s^0 \rightarrow J/\psi f_0(980)$ is an interesting decay mode since it can allow a measurement of the strong CP-violating phase in $B^0_s$ mixing, $\phi_s$.

A measurement of the relative branching fraction using approximately 8 fb$^{-1}$ of data yields:

$$R = \frac{\mathcal{B}(B_s^0 \rightarrow J/\psi f_0(980); f_0(980) \rightarrow \pi^+\pi^-)}{\mathcal{B}(B_s^0 \rightarrow J/\psi \phi; \phi \rightarrow K^+K^-)} = 0.210 \pm 0.032 \text{ (stat)} \pm 0.036 \text{ (syst)}.$$

The relative branching fraction of $B_s^0 \rightarrow J/\psi f_0(980)$, $f_0(980) \rightarrow \pi^+\pi^-$ to $B_s^0 \rightarrow J/\psi \phi, \phi \rightarrow K^+K^-$ should be large enough to allow a measurement of $\phi_s$ using the decay $B_s^0 \rightarrow J/\psi f_0(980)$. An analysis to measure $\phi_s$ using the decay $B_s^0 \rightarrow J/\psi f_0(980)$ is currently being pursued.

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APPENDIX A: VARIABLES USED IN BDT

- 6 Isolation variables for $B_s^0$ computed using different choices of $\Delta R$ and different choices for which particles were included in the isolation cone.
- Total momentum of $B_s^0$ before the correction due to the mass constraint of $J/\Psi$.
- $p_T$ of $B_s^0$ before the correction due to the mass constraint of $J/\Psi$.
- $\chi^2$ of $B_s^0$ vertex fit.
- $J/\Psi$ mass.
- Total momentum of $J/\Psi$.
- $p_T$ of $J/\Psi$.
- Total momentum of leading kaon (pion).
- $p_T$ of leading kaon (pion).
- Total momentum of trailing kaon (pion).
- $p_T$ of the trailing kaon (pion).
- Total momentum of leading muon.
- $p_T$ of leading muon.
- Total momentum of trailing muon.
- $p_T$ of trailing muon.
- Total momentum of $\phi$ ($f_0(980)$).
- $p_T$ of $\phi$ ($f_0(980)$).
- Maximum of $\chi^2$ of the vertex fit formed by $J/\Psi$ and a kaon (pion).
- Maximum of $\chi^2$ of the kaons (pions) track fit.
- Maximum of $\Delta R$ of the kaons (pions) to the $B_s^0$ momentum.
- Maximum of $\Delta R$ between a muon and $B_s^0$.
- Maximum of $\chi^2$ vertex fit of $J/\Psi$ and $\phi$ ($f_0(980)$).
- Minimum of $\chi^2$ of the vertex fit formed by $J/\Psi$ and a kaon (pion).
- Minimum $\chi^2$ of kaons (pions) track fit.
- Minimum of $\Delta R$ between kaon (pion) and $B_s^0$.
- Minimum of $\Delta R$ between muon and $B_s^0$.
- Minimum of $\chi^2$ vertex fit of $J/\Psi$ and $\phi$ ($f_0(980)$).
- Transversity angle $\varphi$.
- Transversity angle $\cos \theta$.
- Transversity angle $\cos \psi$.
- $1-\sin^2 \varphi \cos^2 \theta$. 