Estimating precipitation on early Mars using a radiative-convective model of the atmosphere and comparison with inferred runoff from geomorphology

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Abstract

We compare estimates of atmospheric precipitation during the Martian Noachian-Hesperian boundary 3.8 Gyr ago as calculated in a radiative-convective column model of the atmosphere with runoff values estimated from a geomorphological analysis of dendritic valley network discharge rates. In the atmospheric model, we assume CO\textsubscript{2}-H\textsubscript{2}O-N\textsubscript{2} atmospheres with surface pressures varying from 20 mb to 3 bar with input solar luminosity reduced to 75\% the modern value.

Results from the valley network analysis are of the order of a few mm d\textsuperscript{-1} liquid water precipitation (1.5-10.6 mm d\textsuperscript{-1}, with a median of 3.1 mm d\textsuperscript{-1}). Atmospheric model results are much lower, from about 0.001-1 mm d\textsuperscript{-1} of snowfall (depending on CO\textsubscript{2} partial pressure). Hence, the atmospheric model predicts a significantly lower amount of precipitated water than estimated from the geomorphological analysis. Furthermore, global mean surface temperatures are below freezing, i.e. runoff is most likely not directly linked to precipitation. Therefore, our results strongly favor a cold early Mars with episodic snowmelt as a source for runoff.

Our approach is challenged by mostly unconstrained parameters, e.g. greenhouse gas abundance, global meteorology (for example, clouds) and planetary parameters such as obliquity - which affect the atmospheric result - as well as by inherent problems in estimating discharge and runoff on ancient Mars, such as a lack of knowledge on infiltration and evaporation rates and on flooding timescales, which affect the geomorphological data. Nevertheless, our work represents a first step in combining and interpreting quantitative tools applied in early Mars atmospheric and geomorphological studies.

Keywords: early Mars: habitability, precipitation, atmospheres, geomorphology

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1. Introduction

Habitability defined as the conditions suitable for life (e.g., Mars Exploration Program Analysis Group 2005) has become a central concept in both Solar System and exoplanet science. Early Mars is arguably the key environment to study whether habitable conditions could arise away from the Earth.

In this work we apply an atmospheric model to estimate global mean precipitation rates on early Mars. These are then compared with runoff rates as derived from a geomorphological data analysis of a sample of valley networks. Our main aim is not to investigate the formation of individual networks. Rather, we aim to assess (i) the probable strength of the overall hydrological cycle on early Mars in terms of the amount of precipitated water needed to form the networks, and (ii) whether the atmospheric conditions would have allowed for such a hydrological cycle, again in terms of amount of precipitated water, but also in terms of temperature (snow vs. rainfall).

We begin (Section 1.1) by discussing processes affecting atmospheric formation and composition since these are critical for the early Mars climate hence habitability. Then we give an overview of the geomorphological valley features (Section 1.2) observed on Mars which provide key evidence that early Mars was wet. Section 2 presents the tools used and their constraints. Section 3 presents results, comparing precipitation rates from the atmospheric model with those from the geomorphological approach. Section 4 presents a discussion and Section 5 shows conclusions.

1.1. Background on early Mars Atmosphere

Constraints on atmospheric composition and mass for the early Martian atmosphere can be obtained from a combination of outgassing and escape modeling as well as measurements of e.g. isotopic ratios of nitrogen, oxygen and carbon. Degassing during the early magma ocean phase could have led to an atmosphere of tens of bars or more, but this was probably efficiently removed very fast either during the magma-ocean phase or at the latest during the first few hundred million years due to strong solar activity (e.g., Tian et al. 2009, Lammer et al. 2013). Later input by outgassing is likely insufficient to form dense CO$_2$ atmospheres of the order of a few bars. Model studies suggest a maximum of about 0.5-1.5 bar before 3.8 Gyrs (e.g., Phillips et al. 2001, Grott et al. 2011), with the lower value being more realistic considering the low oxygen fugacity of the Martian mantle and that crustal recycling was inefficient in Mars (e.g., Stanley et al. 2011). However, impacts during the late heavy bombardment may have provided additional atmospheric mass (up to a few bars, e.g., de Niem et al. 2012). Isotopic ratios (e.g., Jakosky and Phillips 2001, Fox and Had 2010, Gillmann et al. 2011) and an in-situ analysis of estimated rock trajectories during explosive volcanic eruptions (e.g., Manga et al. 2012) also suggest a denser atmosphere than today. Upper limits on early Mars atmospheric pressure of about 1 bar have been reported recently based on crater analysis (Kite et al. 2014). A key challenge is how to remove considerable amounts of atmosphere in order to arrive at the present, thin atmosphere, since loss processes are not thought to be efficient after the Noachian period (e.g., Lammer et al. 2013).
The early Mars atmosphere is thought to be composed mainly of CO$_2$, as suggested by outgassing models (e.g., Phillips et al. 2001), although such studies also predict significant H$_2$O outgassing (e.g., Grott et al. 2011). Trace gases could have been present in the atmosphere, e.g., SO$_2$ due to volcanic outgassing (e.g., Farquhar et al. 2000, Halevy et al. 2007) or O$_3$ due to atmospheric photochemistry (e.g., Selsis et al. 2002). Atmospheric N$_2$ may have been present since its original inventory is relatively large (e.g., McKay and Stoker 1989). Other radiatively active gases such as CH$_4$ have also been suggested (e.g., Postawko and Kuhn 1986). Recent studies investigated the possibility of H$_2$-induced warming (e.g., Ramirez et al. 2014) because H$_2$ could have been a major atmospheric constituent due to enhanced outgassing from the reduced early Mars mantle. However, most atmospheric model studies only investigated CO$_2$-H$_2$O scenarios, some with the addition of either SO$_2$, H$_2$ or N$_2$, but currently no model has used a combination of all of these gases.

Early 1D CO$_2$-H$_2$O atmospheric model studies by, e.g., Kasting (1991) suggested mean surface temperatures far below freezing, indicating that sustained rainfall might not be the reason for producing observed fluvial features. One possible mechanism suggested for warming early Mars includes the formation of CO$_2$ clouds (e.g., Pierrehumbert and Erlick 1998, Forget and Pierrehumbert 1997). However, 1D and 3D modeling studies suggested that the cloud cover would have to be nearly 100% (e.g., Mischna et al. 2000), which is unrealistic as found by more detailed, time-dependent 1D or 3D simulations (e.g., Colaprete and Toon 2003, Wordsworth et al. 2013). Recent radiative transfer modeling studies (Kitzmann et al. 2013) suggested that the overall warming effect might have been strongly overestimated.

Most recent 1D atmospheric modeling studies continue to calculate mean surface temperatures below freezing even when including the presence of additional greenhouse gases such as SO$_2$ (e.g., Tian et al. 2010) or N$_2$ (e.g., von Paris et al. 2013a). In contrast, the new study by Ramirez et al. (2014) found mean surface temperatures well above freezing upon simulating dense CO$_2$-H$_2$ atmospheres. Kahre et al. (2013) speculate that a highly active dust cycle on early Mars could have warmed the surface. Dust could have warmed the surface by up to 10 K depending on dust opacity (Forget et al. 2013). A reduction in surface albedo (e.g. due to a larger exposure of basaltic bedrock) has been suggested to warm the surface by, e.g., Fairén et al. (2012) and Mischna et al. (2013).

With 3D model studies (e.g., Johnson et al. 2008, Wordsworth et al. 2013, Mischna et al. 2013, Urata and Toon 2013), the problem of cold global mean surface temperatures could be addressed to some extent: They showed that even for mean surface temperatures below freezing, large areas of the Martian surface could remain much warmer, with annual means of 260-270 K. In addition, 3D global and mesoscale models of the early Mars climate suggest that orography could be an important factor to drive precipitation. In a recent study, Scanlon et al. (2013) show that orography-driven precipitation in the form of snowfall (of the order of about 10$^{-2}$-10$^{-1}$ kg d$^{-1}$ m$^{-2}$) coincides roughly with the location of former rivers on early Mars.

1.2. Background on Geomorphology: Martian Valley Networks

The term valley networks denotes fluid-carved systems of incisions on planetary surfaces, interpreted to be former river valleys. Less degraded fluvial valleys may
still possess a narrow interior channel along the valley bottom, which represents the riverbed itself (e.g., Jaumann et al. 2005). Valley networks on Mars occur in two generic types, namely “dendritic” and “longitudinal”. Each type implies a different hydrological regime. Dendritic patterns are interpreted to be indicative of precipitation-fed surface runoff due to their analogy to terrestrial features (e.g., Craddock and Howard 2002, Irwin et al. 2005, Barharn et al. 2009, Ansan and Mangold 2013). The surface runoff can be either caused by snowmelt or rain whereby recent studies emphasize that episodic snowmelt might be the most favorable process of water release (e.g., Forget et al. 2013, Wordsworth et al. 2013, Scanlon et al. 2013). Longitudinal valleys may represent fluvial channels, but featuring only a few tributaries.

Whereas some authors propose erosion by groundwater seepage (sapping) as the most plausible water release mechanism for these channels (e.g., Malin and Carr 1999, Goldspiel and Squyres 2000, Harrison and Grimm 2005, Jaumann et al. 2010), others have demonstrated that sapping alone does not account for the erosion at analogous terrestrial channels and a significant contribution by overland runoff is required (e.g., Lamb et al. 2008). Valley networks on Mars occur mostly in the heavily cratered southern highlands whereas some isolated fluvial channels have been observed along the flanks of volcanic edifices (e.g., Gulick and Baker 1990, Carr 1995, Fassett and Head 2006, Hynek et al. 2010).

Crater size-frequency analyses of valley network-incised regions show that fluvial activity peaks during the late Noachian and sharply decreases after the early Hesperian (e.g., Fassett and Head 2008, 2011, Hoke and Hynek 2009). Nevertheless, recent research has shown that aqueous surface processes continued even after the early Hesperian, though on a less intense level (e.g., Fassett et al. 2010, Howard and Moore 2011, Hauber et al. 2013, Parsons et al. 2013, Hobley et al. 2014). A recent study by Buhler et al. (2014) suggests intermittent (not continuous) fluvial activity of the order of $10^{-3}$ of the available time to form the networks, based on complex transport and hydrological analyses.

2. Tools and Methods

2.1. Atmosphere

We use atmospheric profiles of pressure $p$, temperature $T$ and water concentrations $c_{\text{H}_2\text{O}}$ from calculations presented in von Paris et al. (2013a). These profiles were obtained with a 1D steady-state, radiative-convective atmospheric model which simulates globally averaged conditions. The model solves the radiative transfer equation and accounts for convective energy transport in the lower atmosphere by performing instantaneous convective adjustment to the (wet) adiabatic lapse rate. Further details can be found in von Paris et al. (2013a) and references therein. Model atmospheres were assumed to be composed of varying amounts of CO$_2$ (8 values between 0.02-3 bar) and N$_2$ (5 values between 0-0.5 bar). Solar irradiation was set to be consistent with Noachian conditions 3.8 billion years ago, i.e. 75% of today’s irradiation (e.g., Gough 1981).

Figure 1 shows the calculated surface temperatures (black lines) and planetary albedos (red lines). The planetary albedo increases due to enhanced Rayleigh scattering
Figure 1: Surface temperatures (black) and planetary albedo (red) as a function of CO$_2$ partial pressure at two values of N$_2$ partial pressure (plain: 0 bar, dotted: 0.5 bar), values taken from simulations of von Paris et al. (2013a). 273 K indicated by horizontal dashed line. RS=Rayleigh scattering (cooling), GHE=Greenhouse effect (warming).

which scales with atmospheric mass, hence also the higher albedo in the 0.5 bar N$_2$ case. With increasing CO$_2$ partial pressures, both the zero N$_2$ case (plain line) and the 0.5 bar N$_2$ case (dotted line) approximately converge to the same albedo since CO$_2$ is a much more efficient scatterer than N$_2$ (Vardavas and Carver 1984) and dominates the scattering optical depth. Surface temperatures show a distinct maximum. This is because the surface temperature first increases when increasing CO$_2$ due to an enhanced greenhouse effect, reaching 248 K at 2 bar of CO$_2$ and zero N$_2$. Adding 0.5 bar of N$_2$ increases the surface temperature by up to 12 K, depending on CO$_2$ partial pressure. Above (2-3) bars of surface CO$_2$, the greenhouse effect saturates. An opposing, cooling effect via the strong Rayleigh scattering becomes important, and surface temperatures decrease again. This effect is known as the maximum greenhouse effect (e.g., Kasting 1991, Kasting et al. 1993, Tian et al. 2010, von Paris et al. 2013a).

Water concentration profiles as a function of altitude $z$ in von Paris et al. (2013a) were calculated from the following equation:

$$c_{H_2O}(z) = RH(z) \cdot \frac{p_{\text{sat},H_2O}(T(z))}{p(z)} \quad (1)$$

where RH is the Relative Humidity and $p_{\text{sat},H_2O}(T(z))$ the temperature-dependent water saturation vapour pressure. RH is thus defined as the water vapour pressure relative to the saturation vapour pressure and is a measure of the amount of water able to be held in the gas-phase. It depends on e.g. T-p conditions, and (sensitively) to the heterogenous surface loading (dust, aerosol) of the atmosphere (which is not known for early Mars). RH is therefore not well constrained in the early Martian atmosphere. Previous 1D studies usually assumed either a fully-saturated troposphere, i.e. RH=1, or 50% saturation, i.e. RH=0.5 (e.g., Mischna et al. 2000, Colaprete and Toon 2003, Tian et al. 2010). The calculations in von Paris et al. (2013a) also used RH=1. For 1D simulations of modern Earth or hypothetical terrestrial exoplanets, the RH profile is often based on the observed mean Earth profile of Manabe and Wetherald (1967).
From the calculated water profiles of Eq. 1, it is possible to obtain the mean atmospheric water column \( C_{\text{H}_2\text{O}} \) in units of kg m\(^{-2}\), see Figure 3 in von Paris et al. (2013a), via:

\[
C_{\text{H}_2\text{O}} = \frac{m_{\text{H}_2\text{O}}}{\mu} \cdot \sum_{i=1}^{N-1} c_{\text{H}_2\text{O},i}(p_i - p_{i+1})
\]  

(2)

where \( N \) is the number of atmospheric levels (here, \( N=52, i=1 \) at surface), \( g \) the planetary gravity (for Mars, \( g=3.73 \text{ m s}^{-2} \)), \( \mu \) the mean atmospheric weight, \( m_{\text{H}_2\text{O}} \) the molecular weight of water and \( c_{\text{H}_2\text{O},i} \), \( p_i \) water concentrations and pressure in level \( i \).

In atmospheric 1D and 3D models, precipitation is calculated, e.g., by assigning precipitation efficiencies to cloud layers (e.g., Rennó et al. 1994), choosing a precipitation threshold for the water content (e.g., Wordsworth et al. 2013) or simply assuming that clouds at the surface precipitate all super-saturated water (e.g., Segura et al. 2008). In this work, we choose a different approach, as follows. The mean precipitation on Earth is \( \approx 2.6 \text{ mm d}^{-1} \), i.e. \( 2.6 \text{ kg m}^{-2} \text{ d}^{-1} \) (e.g., Xie and Arkin 1997, Mitchell and Jones 2005, Adler et al. 2012). Taking a mean Earth water column of \( C_{\text{H}_2\text{O,Earth}}=19.5 \text{ kg m}^{-2} \) (see e.g., modern Earth atmospheric simulations by Grenfell et al. 2007), this amounts to a daily precipitation rate, \( pr=13.3\% \) of the total water column. In this work we apply this value of \( pr \) (which is clearly a source of uncertainty, see discussion below) to the early Mars scenarios (see Fig. 1) to calculate precipitation rates \( P \):

\[
P = pr \cdot C_{\text{H}_2\text{O}}
\]  

(3)

For example, von Paris et al. (2013a) found, at a CO\(_2\) partial pressure of 2 bar and 0.5 bar of N\(_2\), a water column of 5.2 kg m\(^{-2}\) (see their Fig. 3). The corresponding mean precipitation would then be 0.7 mm d\(^{-1}\), i.e. around 26% of the mean Earth value.

To explore uncertainties in this simple, first-order approach, we perform the following sensitivity studies regarding three important parameters for the calculation of precipitation, i.e. the assumed percentage precipitation \( pr \), the RH profile and the surface temperature:

**Atmospheric Precipitation**

We vary \( pr \) in Eq. 3 assumed for early Mars as follows. On Earth (mean \( pr=13.3\% \)), there is a latitudinal gradient in \( pr \), due to global circulation and the land-ocean distribution. Figure 2 shows the latitudinal gradient of the annual means of water column and precipitation. The values are based on monthly averages for the year 2013, accessed through the NCEP/NCAR (Kalnay et al. 1996) website http://www.esrl.noaa.gov/psd/cgi-bin/data/timeseries/timeseries1.pl. Figure 3 then shows the associated value of \( pr \), using eq. 3. For the most part (except south polar regions, where water column measurements are very uncertain), \( pr \) remains between about 8-30%. Hence, we varied \( pr \) based on the extremes found on modern Earth, i.e. \( pr=8, 13.3 \) and 30%. Idealized 3D simulations by O’Gorman and Schneider (2008) found that the atmospheric water residence time \( \tau_w = 1/pr \) depends on surface temperature and actually increases for warmer climates, broadly consistent with modern Earth observations (see Fig. 3). The actual amount of precipitation depends on the
amount of available water in the atmospheric column as well as the precipitation efficiency \( pr \), which can both be calculated consistently in a 3D model. However, in this work, we only calculate the water column as a function of atmospheric composition and vary \( pr \) within a reasonable range.

Figure 2: Latitudinal gradient of water column (left panel) and precipitation (right panel). 10°-averaged annual mean for year 2013, based on the NCEP/NCAR project (Kalnay et al. 1996). Data set available through [http://www.esrl.noaa.gov/psd/cgi-bin/data/timeseries/timeseries1.pl](http://www.esrl.noaa.gov/psd/cgi-bin/data/timeseries/timeseries1.pl)

How accurate is this approach? Using 3D GCM simulations of early Mars presented by Wordsworth et al. (2013), we estimated their \( pr \) value to be of the order of 20-50% (their Fig. 10 and Table 2), comparable to polar values on Earth (see Fig. 3). This estimate of \( pr \) is obtained as follows: On summing (by eye) the panels describing seasonal snowfall in Fig. 10 of Wordsworth et al. (2013) and using their stated water column of the 1 bar simulation (0.07 kg m\(^{-2}\), see their Table 2), we found a range for \( pr \) of 20-50%. On early Mars, clearly several factors such as the Martian dichotomy will influence global convection, hence the strength of the Hadley cell. Nevertheless these factors are not well defined so our assumption based on the Earth is a reasonable first estimate.

**Atmospheric Relative Humidity**

To investigate uncertainties in early Mars’ RH profiles (see above), we introduced two new RH test cases, namely (i) \( RH=0.5 \) and (ii) \( RH=\text{MW} \), in addition to the original \( RH=1 \) from von Paris et al. (2013a). These three profiles are shown in Fig. 4. Note that although the MW profile drops sharply with altitude, within the lowermost atmospheric scale height (\( \frac{p}{p_{\text{top}}} = 0.36 \), indicated by horizontal line) where most of the water resides, the three RH profiles are rather similar.

We repeated the zero-N\(_2\) simulations with the atmospheric model of von Paris et al. (2013a), using the new RH profiles (i.e., \( RH=0.5 \) and \( RH=\text{MW} \)). The effect on sur-
face temperature was on the order of a few K, comparable to 1D results obtained by Colaprete and Toon (2003). Note that 3D simulations performed by Wordsworth et al. (2013) find a somewhat larger effect of up to 20 K. Water columns decreased by about 30-50% when compared to the RH=1 case, as shown in Fig. 5.

**Surface temperature**

Here, we estimated the effect of a (local) surface temperature increase $\Delta T$ (with respect to the zero N$_2$ scenarios) upon precipitation (see Fig. 12 and discussion there). The surface temperature and the temperature profile are very important factors when calculating precipitation rates because the water vapour saturation pressure $p_{\text{sat, H}_2\text{O}}$, hence the water concentration profile (see Eq. 1), depend strongly on temperature. We add $\Delta T$ to both the surface temperature and the temperature profile from von Paris et al. (2013a). The water profile and the resulting column are then re-calculated with Eqs. 1 and 2. This simplifying approach is justified since most of the water column resides near the surface where the temperature lapse rate is approximately constant with altitude, at about 3-4 K km$^{-1}$, which is close to the dry adiabatic value of 4.3 K km$^{-1}$.

**Global mean vs local precipitation**

There exists not only a latitudinal gradient in mean precipitation (Fig. 2), but also a monthly variation, as shown in Fig. 6. Therefore, at any given location and given time, the actual local precipitation $P_{\text{loc}}$ might not be well represented by the global mean precipitation $P_{\text{glob}}$. Rather, in an extremely simplified approach, one might relate these through

$$P_{\text{loc}} = x \cdot P_{\text{glob}}$$

where $x$ must be determined by temporally and spatially resolved calculations.
However, as indicated by Figs. 2 and 6 on spatial scales resolved by present-day 3D GCM simulations, $x$ is probably not larger than about 3. Mesoscale 3D models of early Mars have shown that orography-driven precipitation can be much stronger (up to an order of magnitude) than synoptic-scale precipitation (Scanlon et al. 2013), suggesting values of up to $x=10$ for increasingly finer spatial resolutions.

In a last parameter variation, we therefore estimated an approximate value for $x$ in order to obtain an agreement between atmospheric model and geomorphology data.

2.2. Geological Constraints

2.2.1. Methods

Most valley networks represent relics of ancient fluvial activity on early Mars near the Noachian-Hesperian boundary. Thus, it is not possible to measure directly discharge rates $Q$ (in units of m$^3$s$^{-1}$). They are instead derived from parameters related to the valley system’s morphometric properties, channel width $W_C$, depth $D$, and the flow velocity $v$:

$$Q = W_C \cdot D \cdot v$$

The depth $D$ of the Martian riverbed is usually not available. It is in most cases too small to be resolved in the Digital Terrain Models (DTM) derived from, e.g. Mars Express’s HRSC (High Resolution Stereo Camera, Jaumann et al. 2007, Gwinner et al. 2010) and Mars Global Surveyor’s MOLA (Mars Orbiter Laser Altimeter, Smith et al. 2001). Furthermore, the flow velocity $v$ is also unknown. Therefore, $Q$ can only be derived based on the channel width $W_C$, which is in principle observable. The lack of reliable information on the stability of the channel banks complicates accurate measurements of $W_C$. However, empirical correlations can be used to estimate discharge rates from the width of the channels. On Earth, for channels in the Missouri river area,
Osterkamp and Hedman (1982) use an empirical power law equation \( Q = f \cdot W_c^e \) to obtain mean discharge rates:

\[
\text{Q}_{\text{Earth,mean}} = f_{\text{Earth}} \cdot W_{\text{Earth}}^e = 0.027 \cdot W_C^{1.71}
\] (6)

The main assumption in this work and others (e.g., Irwin et al. 2005) is that \( Q \) scales with the same power law, meaning the exponent \( e_{\text{Earth}} \) does not change for Martian channels (i.e., \( e_{\text{Earth}} = e_{\text{Mars}} \)). Only the scaling factor \( f_{\text{Mars}} \) will be adjusted to Martian gravity based on the value of \( f_{\text{Earth}} \). To obtain a conservative estimate of the channel width, we follow the approach of Irwin et al. (2005). We use narrow, straight channel sections to measure channel widths. It is assumed that channel bank-to-bank widths are less modified in such areas. Thus, this approach helps minimizing the impact of subsequent mass movements that could heavily modify channel bank-to-bank widths.

To calculate \( f_{\text{Mars}} \), we follow the approach of Irwin et al. (2005) and Moore et al. (2003). They assumed that the channel width \( W \) scales with relative gravity \( g \) (\( = 0.38 \) for Mars/Earth system) as \( g^{-0.23} \). For the same unit discharge \( Q \), since \( e_{\text{Earth}} = e_{\text{Mars}} \), we have then:

\[
f_{\text{Mars}} = f_{\text{Earth}} \left( \frac{g_{\text{Mars}}}{g_{\text{Earth}}} \right)^{-0.23} = 0.018
\] (7)

Inserting into eq. 6 leads to the following empirical relation between \( W \) and \( Q \) on Mars:

\[
Q_{\text{Mars,mean}} = 0.018W_C^{1.71}
\] (8)

Local variations of \( W \) by later erosion and modification processes result in a possible error of a factor of 2; a further factor of 3 may arise via the unknown stability of the banks and is also inherent in the empirical equation itself (Irwin et al. 2005). Thus,
the results for $Q$ are conservative estimates, but are most likely accurate to within an order of magnitude. Once the discharges have been derived, the runoff rate $R$ can then be estimated:

$$R = \frac{Q}{C}$$

where $Q$ is the discharge rate of a valley network at its outlet and $C$ the respective catchment area. This results in a water equivalent layer from a few millimeters up to several centimeters thick per d.

2.2.2. Data set

In total, we used runoff values of 18 valley networks in our analysis, as presented in Table 1. Their distribution is indicated in Fig. 7. It is generally accepted that surface runoff occurred mainly at the transition between Noachian/Hesperian 3.7-3.8 billion years ago and earlier (e.g., Fassett and Head 2008, Hynek et al. 2010). At this time, there was a major decrease in runoff intensity on the Martian surface (Carr and Head 2010). Hence the data set is assumed to be consistent in time with the atmospheric model simulations.

Their channel widths and the corresponding discharge rates have been determined. Where available, direct measurements of $W_C$ have been used to calculate $Q$ via Eq. 8. However, most of these valleys do not show any channels (because they are completely covered with sediment or destroyed by erosion). Hence, channel widths $W_C$ for Eq. 8 have been deduced from the measured valley width $W_V$ via a simple scaling suggested by Penido et al. (2013):

$$W_C = 0.14 \cdot W_V$$
Table 1: Valley networks used in this work (measured quantities in bold).

| Identifier | location | $W_V$ [m] | $W_C$ [m] | $C$ [km$^2$] | $Q_{\text{mean}}$ [m$^3$ s$^{-1}$] | $R_{\text{mean}}$ [mm d$^{-1}$] | $Q_{\text{peak}}$ [m$^3$ s$^{-1}$] | $R_{\text{peak}}$ [mm d$^{-1}$] |
|------------|----------|-----------|----------|-------------|----------------|----------------|----------------|----------------|
| 8604-1     | 38°15' S/203° E | - | 250 | 1840 | 226.8 | 10.65 | 1179.2 | 55.3 |
| 8604-2     | 38°27' S/204° E | - | 220 | 2970 | 182.3 | 5.30 | 1008.9 | 29.3 |
| 8604-3     | 38°30' S/204°5' E | - | 255 | 2230 | 234.6 | 9.09 | 1208.1 | 46.8 |
| H1226_0000 | 1°52' N/89°25' E | 1770 | 247 | 12840 | 222.2 | 1.49 | 712.0 | 7.8 |
| H5212_0000 | 1°49' N/121°16' E | 5850 | 819 | 21240 | 1725.7 | 7.02 | 5015.7 | 20.4 |
| H2081_0000 | 0°15' N/124°12' E | 2070 | 289 | 4240 | 290.6 | 5.92 | 1407.4 | 28.6 |
| H0430_0000 | 36°57' S/7°56' E | 480 | 67 | 300 | 23.8 | 6.87 | 236.5 | 68.1 |
| H2181_0001 | 45°29' S/156°45' W | 1430 | 200 | 3030 | 154.8 | 4.41 | 898.2 | 25.6 |
| H5168_0001 | 10°47' S/156°45' W | 1180 | 165 | 3530 | 111.4 | 2.72 | 710.3 | 17.3 |
| H2689_0001 | 34°40' S/146°04' E | 2120 | 296 | 9070 | 302.8 | 2.88 | 1449.1 | 13.8 |
| H7213_0000 | 12°21' S/177°58' W | 2040 | 285 | 14120 | 283.8 | 1.73 | 1383.6 | 8.4 |
| H2459_0009 | 17°6' S/65°42' E | 2790 | 390 | 15950 | 485.2 | 2.62 | 2028.7 | 10.9 |
| H2457_0000 | 52°49' S/90°49' W | 1880 | 263 | 8400 | 247.3 | 2.54 | 1254.5 | 12.9 |
| H2475_0000 | 49°19' S/65°28' W | - | 160 | 6040 | 105.7 | 1.51 | 684.1 | 9.7 |
| H2475_0003 | 52°26' S/65°51' W | 1030 | 144 | 2430 | 88.3 | 3.14 | 601.6 | 21.3 |
| H4290_0000 | 35°3' S/132° E | - | 270 | 7170 | 258.7 | 3.11 | 1295.3 | 15.6 |
| H2539_0000 | 27°16' S/128°10' E | 1600 | 224 | 1720 | 188.0 | 9.44 | 1031.4 | 51.8 |
| H6438_0000 | 24°54' S/3°26' W | 2880 | 403 | 18230 | 513.2 | 2.43 | 2111.5 | 10.0 |

Table 2: Comparison of peak discharge and runo$ff$ rates.

| Region/name | $Q_{\text{peak}}$ [m$^3$ s$^{-1}$] | $R_{\text{peak}}$ [cm d$^{-1}$] | references |
|-------------|----------------|----------------|-------------|
| global distribution (see Fig. 7) | 236-5015 | 0.8-6.8 | this work |
| global distribution | 300-5800 | 0.1-6 | Irwin et al. (2005) |
| Terra Sabaea, Arabia Terra, Meridiani Plan. | 7,000-70,000 | 0.4-63 | Hoke et al. (2011) |

Subsequently, the sizes of the respective catchment areas $C$ were determined using topographic data based by HRSC and MOLA DTMs (e.g., Gwinner et al. 2010, Smith et al. 2001).

The runoff rates were calculated from Eq. 9, resulting in a mean runo$ff$ of 1.5-10.65 mm d$^{-1}$, depending on valley location. The median value of our dataset is 3.14 mm d$^{-1}$, relatively close to the mean Earth precipitation of 2.6 mm d$^{-1}$. As is apparent from Fig. 2 and Table 1, quite a few valley networks require precipitation rates close to or higher than typical tropical values found on Earth. Overall, therefore, these runoff rates would suggest a very strong, global mean hydrological cycle on early Mars, if the networks indeed formed throughout extended periods of warm climate.

2.2.3. Comparison with previous work

To compare the runoff rates for our networks with rates previously published in the literature, we need to calculate peak instead of mean runoff rates (also shown in Table 1). Note that when comparing to a global mean atmospheric model, as is the aim in
this work, we should use mean runoff rates. In a similar reasoning as for deriving eq. 8, based on the peak discharge approximation from Osterkamp and Hedman (1982) we obtain

$$Q_{\text{Mars, peak}} = 1.4 W^{1.22}$$

(11)

Peak runoff rates from our 18 valley networks are between 0.8 cm d$^{-1}$ and 6.8 cm d$^{-1}$. Irwin et al. (2005) find runoff rates of 0.1 cm d$^{-1}$ to 6 cm d$^{-1}$. In contrast to our study, Hoke et al. (2011) investigated larger valley systems, which results in runoff rates of 0.4 cm d$^{-1}$ to 63 cm d$^{-1}$. In general, our results are in good agreement with the measurements of other investigations of Martian peak runoff rates (see Table 2). In a very recent work, Palucis et al. (2014) estimated discharge (not runoff) from a channel in Gale Crater (average channel width 27 m). They found values ranging from 3.7-6.5 m$^3$s$^{-1}$ when assuming a shallow channel and up to 117-207 m$^3$s$^{-1}$ for deeper channels. This compares reasonably well to estimates from our simple equations 8 (5 m$^3$s$^{-1}$) and 11 (78 m$^3$s$^{-1}$) when using the stated channel width of 27 m.

3. Results

Figure 8 shows our precipitation rates as a function of CO$_2$ partial pressure as inferred from the atmospheric model for the scenarios discussed. Also shown are derived mean runoff rates (horizontal lines) from valley network data (minimum, median and maximum). We show atmospheric scenarios with zero and 0.5 bar N$_2$. The atmospheric model results display a maximum in precipitation rate, as could be expected from Fig. 1.
Figure 8 suggests that the calculated mean precipitation rates are lower by more than an order of magnitude compared to the median mean runoff value derived from the network data. Even the minimum runoff from the valley networks still is roughly 7 times higher than the maximum value calculated from the zero N<sub>2</sub> case.

Figure 9 shows the effect of adopting different relative humidity profiles on the calculated precipitation rate. As expected, since most of the water column lies in the lowermost atmospheric layers, the effect is rather small, even when reducing the RH from RH=1 to the MW RH profile, although it amounts to roughly a factor of 2 decrease compared to the fully saturated RH=1 case.

Figure 10 shows the influence of varying the adopted pr value on precipitation rates. For the lower (Earth) values of pr = 8% the disagreement between atmospheric and geological data becomes stronger, as expected, i.e. a significant additional dis-
agreement of a factor of about three between atmospheric and geological data becomes apparent. Only in the most favorable case (high N₂, high pr) can the atmospheric model reproduce roughly the lowest precipitation value inferred from the valley networks.

Figure 11 shows our favored estimates of early Mars precipitation, with RH=1 and pr=0.3. The use of RH=1 was justified by the absence of any realistic information on the relative humidity distribution on early Mars. Results by Wordsworth et al. (2013) suggest that the atmosphere was most likely significantly drier, therefore we choose RH=0.5 which yields our driest runs (see Fig. 5). The favored estimate of early Mars precipitation is 0.3, which is closer to Earth polar values (see Fig. 3) and estimates from Wordsworth et al. (2013). We also show precipitation estimates with x=10 (taken from Scanlon et al. 2013, see eq. 4).

Figure 11: Most favored estimates of precipitation: RH=0.5, pr=0.3, for different values of x.

It is clearly seen that in this case, the disagreement between global mean atmospheric and valley network data remains substantial. However, for large values of x,
estimated amounts of precipitated water become somewhat closer to each other. Still, it is unclear which mechanisms would drive \( x \) to the needed values of \( x > 10-20 \) (or even higher at lower CO\(_2\) pressures). This remains a question for future work.

4. Discussion

4.1. Runoff from rain or snowmelt?

The aim of this work has been to compare precipitation rates calculated with a 1D atmospheric model to runoff rates inferred from geomorphological data. For this comparison to be meaningful, one critical condition must be fulfilled, i.e. precipitation \( P \) is the source for runoff \( Q \).

As is apparent from Fig. 1, calculated global mean surface temperatures are far below freezing, hence \( P \) would mainly occur as snowfall than as rain (Wordsworth et al. 2013) and therefore would not be linked directly to \( Q \). Numerous studies suggest a possibly significant contribution by snowmelt (e.g., Clow 1987, Kite et al. 2013, Wordsworth et al. 2013, Palucis et al. 2014), when orbital elements are suitable. Hence, snowmelt rather than precipitation may have been the dominant factor in producing liquid water available for runoff. Snow melt is a highly time-dependent process, and will concentrate discharge in river channels over short periods of time in spring and early summer (or whenever orbital elements favor local melt conditions), whereas discharge is much lower in the rest of the year (e.g., Bavay et al. 2009). On Earth, runoff over the majority of the land area in the northern hemisphere is seasonally variable (Weingartner et al. 2013) and dominated by snowmelt (e.g., Ferguson 1999, Barnett et al. 2005). This effect is particularly pronounced in arctic regions (e.g., Woo 2012), which may be considered terrestrial climatic analogs to early Martian environments. The hydrograph of arctic rivers displays a peak discharge during snowmelt season (e.g., Woo 1986, Bøggild et al. 1999), and it is this peak discharge which would be responsible for the channel-forming flood. However, we lack the knowledge as to how channel dimensions controlled by snowmelt and associated peak discharges can be used to infer annual mean precipitation rates on Mars.

In summary, the condition of liquid-water precipitation is unlikely to be fulfilled. Therefore, besides the obvious discrepancy in the amount of precipitated water (e.g., Fig. 8), the fact remains that early Mars was most likely too cold to sustain network formation by continued liquid-water precipitation.

4.2. Uncertainties in surface temperature calculations

Figure 12 shows the mean precipitation as a function of CO\(_2\) partial pressure and \( \Delta T \). It is clearly seen that even for denser atmospheres of the order of several bars, the \( \Delta T \) value required for agreement in precipitation between the atmospheric model and the network data (i.e., precipitation \( > 1.5 \text{ mm d}^{-1} \), see Fig. 8) is still of the order of 40-50 K. How could such high temperatures be achieved?
4.2.1. Numerical uncertainties

Firstly, atmospheric models, hence predictions of surface temperature and precipitation, are subject to (numerical) uncertainties.

An important aspect is the radiative transfer, hence the strength of the greenhouse effect. Usually, atmospheric models do not solve the radiative transfer equation with a line-by-line code to save computational speed. They instead use faster approximations such as exponential sums or correlated-k methods (e.g., Wiscombe and Evans 1977, Goody and Yung 1989). It can be shown that such methods are quite accurate (e.g., Goody et al. 1989, West et al. 1990, Lacis and Oinas 1991), and most atmospheric models compare well to high-resolution radiative transfer calculations (e.g., Goldblatt et al. 2009, Wordsworth et al. 2010a, Ramirez et al. 2014). The impact on surface temperature is probably small, of the order of 1-2 K at most. The opacity databases which are typically employed, such as Hitran and Hitemp, have evolved quickly in recent years (e.g., Rothman et al. 2009, Rothman et al. 2013), and the effect on radiative-convective calculations can be quite important (e.g., Pavlov et al. 2000).
Especially the treatment of line and continuum absorption of CO$_2$ is another uncertainty factor for early Mars calculations (e.g., Halevy et al. 2009, Wordsworth et al. 2010a, Mischna et al. 2012). Numerical issues, such as the vertical discretization of the atmospheric column, can also introduce uncertainties in surface temperature of a few K for optically thick atmospheres ($p_{CO_2} \geq 0.2$-0.5 bar). In the model used here, a warming effect of up to 7 K was observed upon increasing the number of levels in the troposphere where the opacity is largest. This effect is comparable to other 1D radiative-convective models (e.g., Tian et al. 2010, Kopparapu et al. 2013). For atmospheres with less CO$_2$ partial pressure, the vertical discretization is not important for the calculation of surface temperatures. In summary, we should probably assign an inherent uncertainty of 5-10 K to the calculation of mean surface temperatures. Figure 12 suggests that by using these uncertainty estimates, the discrepancy between geological data and atmospheric model estimates could increase or decrease by about 20%.

4.2.2. 1D vs 3D models

The 1D atmospheric model used in this work calculates annualmean, global mean temperatures. However, the networks mostly formed at lower latitudes where conditions were likely warmer than such global mean values. Indeed, 3D modeling studies (e.g., Wordsworth et al. 2013, Urata and Toon 2013) have suggested that the latitudinal temperature gradient in mean surface temperature is of the order of up to 20-30 K. However, this is below the needed threshold inferred from Fig. 12.

Seasonal or obliquity effects could be much stronger (see e.g., Fig. 3 in Wordsworth et al. 2013), with temperature effects of the order of 50-60 K in some locations. Therefore, a viable alternative to a continuously wet early Mars are scenarios where obliquity cycles allow for periodic warming at the networks' geographic location which would then allow for formation and precipitation of liquid water (Wordsworth et al. 2013). This issue should be investigated with geological constraints on the valley network formation timescales. These are poorly constrained, but it seems that at least a somewhat sustained presence of water was required to form them (Ansan and Mangold 2013).

We acknowledge the importance of full 3D atmospheric studies, demonstrated for many Solar System objects, e.g. for Earth, Mars, Titan etc. However, 1D and 3D studies can be used complementarily to investigate different aspects of atmospheric processes. For example, 1D models of Titan have been used to tackle specific problems of the thermal structure (e.g., McKay et al. 1989) or haze formation (e.g., Lavvas et al. 2008a, Lavvas et al. 2008b), whereas 3D models of Titan are used to address especially the problem of (equatorial) superrotation (e.g., Hourdin et al. 1995, Friedson et al. 2009, Newman et al. 2011, Lebonnois et al. 2012). For early Mars, 1D-2D models have been used to investigate mean surface temperatures and assess the validity of greenhouse solutions (e.g., Postawko and Kuhn 1986, Pollack et al. 1987, Kasting 1991, Mischna et al. 2000, Colaprete and Toon 2003, Tian et al. 2010, Fairén et al. 2012, von Paris et al. 2013a). 3D models have demonstrated the importance of obliquity and transport effects (e.g., Johnson et al. 2008, Forget et al. 2013, Wordsworth et al. 2013, Mischna et al. 2013, Urata and Toon 2013, Scanlon et al. 2013).

It is clear that 3D models are physically more consistent than 1D models since they better resolve the planetary surface, include clouds and horizontal as well as vertical en-
ergy transport by winds or tracer species such as water. However, they introduce many
parameters, some of them even on a sub-grid scale, hence parameterizations are needed
(e.g., leaf area index, Fraedrich et al. 1999, or surface roughness, Wordsworth et al.
2013). Other parameters include, e.g., precipitation efficiencies or precipitation thresh-
olds, cloud properties and the amount of cloud nuclei (e.g., Wordsworth et al. 2013).
Most of them are not known for early Mars.

On applying 3D models, one should always bear in mind that the boundary condi-
tions might so uncertain that one could be simulating conditions which are very different.

In contrast, 1D models somewhat keep the number of parameters under control. In
our model as used for the current manuscript, effectively, the only parameters are the
choice of surface albedo and the choice of the RH profile.

In addition, the current spatial latitude-longitude resolution of most 3D GCM stud-
ies of early Mars (e.g., 32x24 or 32x32 in Wordsworth et al. 2013 and Forget et al.
2013) is insufficient to resolve individual networks. Therefore, even 3D GCM simula-
tions would probably not be enough to address the question of local precipitation for
individual networks.

As stated in the Introduction, we aim at assessing the general strength of the early
Mars hydrological cycle, and not individual network channels. Therefore, the choice
of a 1D model is not thought to severely impact our conclusions.

Ideally, for Early Mars, one would apply both 3D snapshots of the obliquity cycle
to investigate the detailed feedback mechanisms, as well as 1D studies to investigate
a wide parameter range (of e.g. atmospheric composition) not possible in 3D. In our
present work, a 1D study is used to provide only basic indications of the hydrologic
cycle, which in turn depend on obliquity etc. Such a two-pronged approach (i.e. com-
plimentary 1D and 3D studies) could in our opinion prove beneficial for Early Mars.

4.2.3. Atmospheric composition

In the global mean, von Paris et al. (2013a) suggested that 500 mbar of N₂ would
provide about 10 K surface warming. Other candidates for providing surface warming
are additional greenhouse gases such as CH₄ and SO₂ (e.g., Postawko and Kuhn 1986,
Yung et al. 1997, Johnson et al. 2008, Tian et al. 2010, Mischna et al. 2013). However,
an unresolved question is the possible formation of aerosols due to high SO₂ concen-
trations. Like O₃ (a possible by-product of CO₂ photochemistry, e.g. Selsis et al. 2002),
SO₂ is a strong UV absorber. This could help to avoid the surface cooling due to
CO₂ Rayleigh scattering observed at high surface pressures, since SO₂ or O₃ absorp-
tion bands would strongly reduce the planetary albedo (e.g., von Paris et al. 2013b).
Furthermore, together with near-IR CH₄ absorption, such trace gases would probably
warm the lower stratosphere such that CO₂ cloud formation would be largely inhib-
ited, thus reducing the cloud radiative forcing. Volcanic gases such as H₂ could also
play a role in warming early Mars since collision-induced absorption could provide
a large greenhouse effect, and Rayleigh scattering of H₂ is far less efficient than for
CO₂ (e.g., Stevenson 1999, Pierrehumbert and Gaidos 2011, Wordsworth et al. 2011,
Wordsworth and Pierrehumbert 2013, Ramirez et al. 2014). The study of Ramirez et al.
2014 found mean surface temperatures at high CO₂ partial pressures which are com-
patible with the network data presented here.
4.3. Uncertainties in the estimation of discharge and runoff

Our estimates of discharge and the inferred precipitation rates are subject to large uncertainties. The simple assumption that discharge rates can be used to directly estimate precipitation rates neglects many important factors that control this relationship. In this section we address some of the uncertainties that are necessarily involved in attempts to reconstruct the water budget in a 3.8 Gyr-old catchment.

4.3.1. Discharge calculations

Previous studies used different approaches to estimate paleodischarges of Martian channels. Ideally, reliable estimates of paleodischarge would require not only the measurement of morphometric properties of channels, but also the knowledge of or at least well-constrained assumptions of other, independent parameters such as particle size distributions of mobilized sediment and channel floor roughness (see review by Kleinhans 2005). The input parameters for such micro-scale or hydraulic methods are usually poorly known for modern Mars, since they cannot be easily obtained from orbit. However, they can be measured in situ by rovers such as MSL/Curiosity, which landed on the distal parts of an alluvial fan in Gale Crater. For example, the size distribution of rounded and fluvially transported particles was determined by Yingst et al. (2013). The flow velocity, water depth, and discharge of channels that transported the particles that now form outcrops of conglomerate was estimated by Williams et al. (2013). Nevertheless, the data limitations for most other Martian channels imply that macro-scale or hydrologic methods need to be applied for paleodischarge estimates (see Burr et al. 2010). Such form-discharge approaches are based on morphological parameters that are relatively simple to measure and have been used extensively (e.g., Irwin et al. 2005, Williams et al. 2013). It is important to note, however, that gravity effects (e.g., on channel geometry) and the unknown strength of channel banks on Mars introduce significant errors to our paleodischarge estimates (Williams et al. 2013). Moreover, as mentioned, since we usually cannot measure the channel width, we use an empirical relation of channel width to valley width (see Eq. 10).

From eq. 9, the uncertainty \( R \) of the calculated runoff is given by

\[
\left( \frac{\Delta R}{R} \right)^2 = \left( \frac{\Delta C}{C} \right)^2 + \left( \frac{\Delta Q}{Q} \right)^2
\]

The uncertainty \( \Delta Q \) is partly due to the measurement error \( \frac{\Delta W}{W} \) associated with the channel or valley width. However, a very significant part is also contributed by uncertainties due to the application of the approximative eqs. 6 (\( U_6 \), for deriving discharges) and 10 (\( U_{10} \), for deriving channel widths). Combining these, we find

\[
\left( \frac{\Delta R}{R} \right)^2 = \left( \frac{\Delta C}{C} \right)^2 + \left( 1.71 \cdot \frac{\Delta W C}{W C} \right)^2 + U_6^2 + U_{10}^2
\]

For a conservative estimate of a 20 \% error in the measurements of both catchment area and channel width, and taking \( U_6=0.79 \) (standard error for applying the power law of eq. 6 to discharge calculations, Table 3 in Osterkamp and Hedman 1982) and \( U_{10}=0.1 \) (interquartile range for the proportionality constant in eq. 10, Penido et al. 2017)
we thus assign a $1\sigma$ error of 90% to the calculated runoff. Note that this
neglects any potential systematic uncertainty from applying eq. [10] implying that our
runoff uncertainty estimates are probably optimistic.

Figure 13: Median network runoff (plain line) with its $1\sigma$ error of 90%, (dashed lines) compared to total
model precipitation (mm d$^{-1}$) with nominal values of RH=1 and $pr=13.3\%$. Black: No $N_2$, red: 0.5 bar $N_2$.

Figure 13 shows the effect of this error estimate on the comparison between atmo-
spheric model precipitation and derived network runoff. For high-pressure atmospheres
with significant amounts of $N_2$, both data sets seem to compare roughly within error
bars. Note, however, that our 1D steady-state model atmospheres predict snowfall
rather than rainfall (see surface temperatures in Fig. 1), hence, the associated runoff
would be zero.

Another error source stems from the fact that the approximation formulae provided
by Osterkamp and Hedman [1982] were derived for the Missouri river basin. For other
basins, such formulae will probably differ, although, as stated by Osterkamp and Hedman
[1982], a large number of individual river channel were included in the analysis. There-
fore, data are expected to cover a wide range of channel widths and discharge values,
and the total scatter is probably not much larger than the already stated 79%.

4.3.2. Role of evaporation and infiltration
The derivation of precipitation rates from channel discharge rates (assuming the
channel banks are full) is far from being straightforward. First, the area of the catch-
ment must be known, the shape of which may have been changed by erosion or tec-
tonic deformation in the last $\sim$3.8 Gyr. Additional uncertainties may arise from data
limitations during the mapping process [Penido et al. 2013]. Second, drainage in a
channel does not directly correspond to runoff or precipitation in its catchment area.
If discharge is used to infer precipitation rates, the relative roles of evaporation and
infiltration need to be considered (transpiration does not exist on Mars since there is no
vegetation). In general, the water balance in a catchment system can be expressed as
\[ \Delta S = P - Q_s - Q_G - ET \]  

(14)

where \( \Delta S \) is the change in the amount of water stored in the system, \( P \) is rainfall, i.e. liquid water precipitation, \( Q_s \) is surface discharge, \( Q_G \) is groundwater discharge, and \( ET \) is evapotranspiration. For practical purposes, the amount of water in a system is often assumed to be constant. In terrestrial hydrological studies, infiltration is often considered to be negligible (Anderson and Anderson 2010), since the infiltrated water returns to the stream system as groundwater. If the overall climate is cold (Wordsworth et al. 2013) and the substrate in which a channel is incised is subject to permafrost, the infiltration rate would even tend towards zero, because a permafrost ground would, to a first order, be impermeable (see also Heldmann et al. 2005). Applying the same logic to Mars, we can thus consider Eq. 14 to be equivalent to

\[ \int (R - E) dt = \frac{1}{A} \int Q_s dt \]  

(15)

with \( R \) is the rainfall rate, \( Q_s \) the hydrograph and \( A \) the area of catchment. Evaporation and sublimation rates on modern Mars have been estimated by several past studies. Chittenden et al. (2008) determined sublimation rates of pure water ice as a function of temperature, wind speed, and relative humidity. They found that temperature is the main factor influencing the sublimation rate. The results of Chittenden et al. (2008) show sublimation rates of less than a millimeter per hour (see Table 2 of Chittenden et al. 2008). Whereas these results apply to water ice, Sears and Moore (2005) performed laboratory experiments with a 7 mbar CO\(_2\) atmosphere at 0°C and obtained evaporation rates of 1.01±0.19 mm h\(^{-1}\). After a correction for gravity effects, Sears and Moore (2005) predict evaporation rates on Mars of 0.73±0.14 mm h\(^{-1}\). If one assumes that runoff took place in a rather cold environment on early Mars (Wordsworth et al. 2013), then both sublimation of ice and evaporation of liquid water may have occurred. The effect of thin water ice layers with temperatures around the freezing point of water were investigated by Moore and Sears (2006). These authors find evaporation rates of 0.84±0.08 mm h\(^{-1}\) and 1.24±0.12 mm h\(^{-1}\) with and without a thin ice layer, respectively, and conclude that the presence of thin water ice layers does not have a significant effect on the evaporation rates. The corresponding values for a whole day are 2.02 and 2.98 cm d\(^{-1}\) with and without a thin ice layer, respectively. These rates are of the same order of magnitude as those obtained from discharge estimates, and therefore have to be taken into account and need to be added to the discharge-derived rate before calculating precipitation rates. Of course, the catchment would not be a free surface of water, in which case evaporation rates may be somewhat lower than those obtained for free water surfaces, but in any case the amount of evaporated water would not be negligible.

Another question is whether the assumption of insignificant infiltration in Eq. 14 is valid. The upper crust in the southern highlands, where the valley networks are observed, probably consists of heavily cratered regolith. Such substrate would be characterized by high infiltration capacities that may have impeded runoff production (e.g., Baker and Partridge 1986, Gulick and Baker 1990, Grant and Schultz 1993, Carr and Malin 2000, Irwin et al. 2008 and references therein). In a study of a terres-
trial analogue on Hawaii at the Kilauea and Ka`u deserts, which are characterized by brecciated basaltic material. Craddock et al. (2012) estimate that runoff can only be generated if precipitation rates are >2.5 cm h\(^{-1}\). Infiltrated water would feed groundwater aquifers, which in turn may have contributed to the generation of sapping valleys by groundwater seepage. Groundwater flow, however, may have been different to surface runoff and its associated catchment areas, and it is unclear how to quantify this effect. Since the mean annual temperatures indicated by our study (Fig. 1) and previous modeling of early Mars temperatures (Wordsworth et al. 2013) are below 0°C, we assume permafrost conditions in our hydrologic estimates and therefore neglect the effects of infiltration, including the possible (but minor) infiltration of snow melt into frozen ground.

The above comparison between geomorphologic data and atmospheric models (see e.g., Fig. 8) explicitly assumes no infiltration and no evaporation, i.e. all precipitated water would feed the valley network runoff. Even under such optimistic assumptions, there is a disagreement between both methods. Hence, it is clear that a more detailed analysis, taking into account the full eq. 14 would most likely lead to a larger disagreement. However, given the uncertainties in runoff estimates (see Fig. 13), a full hydrological analysis is probably not warranted by the current data quality.

4.4. Dry warm Mars?

Mean surface temperatures above freezing (warm Mars) do not necessarily lead to high precipitation (wet Mars). Paleoclimatic studies of the Earth during phases of large super-continents imply that the continental climate during these phases might have been very dry (Parrish 1993). This suggests that another condition for extensive precipitation on early Mars would be the presence of large standing bodies of liquid water. 3D climate studies of, e.g., Soto (2012) suggest that without a large ocean, early Mars would have been extremely arid even if it was warm. The existence of a Noachian ocean is currently debated. Several studies however advocate that the northern lowlands have been at least partly ocean-covered (e.g., Clifford and Parker 2001, Perron et al. 2007, Dibiase et al. 2013, De Blasio 2014). If indeed such a large ocean would have existed, precipitation on a warm early Mars would have been abundant (Soto 2012).

4.5. Limits to evaporation

Liquid-water precipitation must be balanced by evaporation of surface water into the atmosphere, otherwise the water column will deplete quickly. Evaporation then leads to a cooling of the surface through the release of latent heat (e.g., Fraedrich et al. 1999). In the model used here, this latent heat flux \(F_{\text{lat}}\) is neglected, and the surface energy balance is only determined by the radiative flux \(F_{\text{rad}}\). However, for increasing amounts of evaporation, the contribution of \(F_{\text{lat}}\) can become significant, and the surface energy balance should read as

\[
F_{\text{surf}} = F_{\text{rad}} + F_{\text{lat}}
\]

The radiative flux in eq. 16 is determined by the net stellar flux reaching the surface and the radiative longwave cooling (i.e., downwards-upwards longwave fluxes). It is calculated directly in the atmospheric model.
For high-pressure atmospheres, the greenhouse effect becomes strong, and the longwave cooling is close to 0 (see von Paris et al. 2013a). For surface pressures higher than about 0.5 bar, the surface radiative flux is almost entirely dominated by the stellar flux.

The right panel of Fig. 14 shows the latent heat flux of the precipitation rates as taken from Fig. 8 assuming a latent heat of 2,500 J g$^{-1}$. It is clearly seen that except the high-CO$_2$ runs ($p > 1$ bar), the value of $F_{lat}$ is somewhat negligible, justifying the model assumption of taking only the radiative flux into account.

In an approach similar to O’Gorman and Schneider (2008), the left panel of Fig. 14 shows the maximum of global mean precipitation, if the entire net surface radiative flux of the model atmospheres would be used to evaporate water. Also indicated are the values of precipitation from Table II. Furthermore, the dotted horizontal line shows the absolute global mean maximum of precipitation ($\approx 3.8$ mm day$^{-1}$), if the entire top-of-atmosphere incoming stellar flux ($\approx 109$ W m$^{-2}$) would be available for surface water evaporation. This is equivalent to assuming a zero-albedo atmosphere (no absorption or scattering of radiation), which is clearly not realistic, as indicated in Fig. 1. Furthermore, longwave cooling as well as surface reflectivity would have to be zero as well, which would be mutually inconsistent. In addition, such a scenario would need a global ocean which is questionable (see discussion above in Sect. 4.4).

Figure 14: Left: Maximum global mean precipitation based on surface energy balance. Network maximum, minimum and median indicated by dot-dashed horizontal lines. Dotted horizontal line indicates maximum precipitation for zero-albedo atmosphere. Right: Latent heat flux of precipitation rates from Fig. 8.

In summary, these calculations suggest that the maximum global mean precipitation sustainable under the faint-Sun conditions assumed for early Mars is about 1.8 mm day$^{-1}$ (Fig. 14 left panel). This is still much less than inferred precipitation from the valley network analysis. Accounting for a latitudinal or seasonal gradient in precipitation compared to a global mean (see discussions above and eq. 4), this could have been enough to sustain valley network formation, even if barely for the highest-runoff channels. However, given that such an amount of precipitation requires that all of the stellar energy reaching the surface be converted into latent heat, these highest-runoff channels were probably not formed during long, continuously wet periods.
5. Conclusions

In this work, we have estimated runoff rates for 18 Mars valley networks and compared them to estimated precipitation rates from an atmospheric model of early Mars. Model atmospheres were composed of varying amounts of CO$_2$ and N$_2$. We also varied parameters such as atmospheric relative humidity and precipitation efficiency to estimate their impact on precipitation values.

Runoff rates inferred from valley network data and precipitation from the atmospheric model generally disagree by about an order of magnitude for high-pressure CO$_2$ atmospheres, the runoff rates being much larger than the atmospheric model precipitation rates. At low CO$_2$ partial pressures, a scenario favored by escape models, the discrepancy is even larger. This suggests that early Mars was probably not a continuously wet environment. Rather, these results point to sporadic periods of high precipitation, probably due to a change in obliquity, or, more likely, (local) melting events where a large snow/ice reservoir accumulated over a geologically long time (e.g., an obliquity cycle) could have melted in a short period. Even though such a conclusion is not new, it is the first time that both geological and atmospheric modeling approaches have been used to test quantitatively the hypothesis of wet versus dry early Mars.

Geological runoff rates are uncertain by currently at least 90\% and atmospheric models are also subject to uncertainties. Therefore, quantitatively comparing the estimates of the amount of precipitated water from both approaches is challenging. However, since global mean surface temperatures as calculated by our atmospheric modeling are far below freezing, calculated model precipitation is most likely not a good predictor of valley network runoff. This points the direction of future research, i.e. the need to better constrain estimates of paleo-discharges in ancient river networks on early Mars, determine the water source for runoff (e.g., snowmelt or rain) and its timescales and refine mesoscale atmospheric modeling of early Mars climate before more rigorous conclusions can be drawn.

Nevertheless our study represents an important first step in constraining precipitation on early Mars involving both the atmospheric and geological communities.

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