A Time Efficient Approach for Quick Splitting and Finding Maximum Matches Sequences in Bio-sequence Analysis

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ABSTRACT
DNA sequence analysis & comparison computation is a vital task in terms of memory & time which is used huge size of data set for biological research. Perfectly aligned sequence find out the matching point or mismatches between two sequences. Our proposed algorithm is composed of two major part. The first part is Fast Splitting(FS), a “Recursive technique” based algorithm which divides the source sequence in appropriate and exact length according to the preference of target sequence. Second part is Fast_Maximum Matches Subsequence Finder(Fast_MMSS). It builds the specialized successor table according to the identical characters of two strings (TLSS & Target Sequence). Then using some special pruning condition, we get the final MMSS. In previous work, dynamic programming and some sorts of Brute force techniques are applied which are faster in terms of time but requires huge memory, while our proposed algorithm maintains the “Time and Space” tradeoff.

Keywords  
Fast Splitting (FS), Maximum Matches Subsequences (MMSS), Target Length Splitted Sequence (TLSS), Successor Table.

1. INTRODUCTION
Bioinformatics is a cross field that retrieves information from the bio-sequences. Bio-sequence analysis leads to identify the similarities, matches or mismatches, alignments between various sequences. Sequence alignment or finding similarities between two sequences leads to identify the bio-logical identity of various species, drug design, and disease identification etc. For finding similarities, there are two types of alignment: Local and Global[13]. Local alignment firstly, takes a portion (substring) of the source sequence and then tries to match with the target sequence. But in Global alignment we take the whole source sequence and try to make an end to end comparison with the target sequence[14]. The sequences which are locally optimal, these are must be globally optimal. There are a lot of evolutionary methods used in various genome projects which can handle a large scale of biological data. Alignment of sequence is the initial state of every genome project. The common matching or similarities indicates the evidence of common genome similarity and homologous relationship. So the alignment of the sequence or finding maximum matched sequence is the vital part for genome projects. There are a lot of algorithms for sequence alignment which are used dynamic programming[16], pruning[17], parallel implementation techniques[18] and recursive backtracking techniques [12]. But using these techniques it is difficult to maintain the ‘Time and Space trade-off’. Because dynamic programming reduces the time but takes huge memory for memorization technique.

First algorithm is the BLAST [1]. They proposed a shared memory version which can easily compute the local optimality. But the main limitation is that it can only search for a single query. Needleman–Wunsch[2] proposed a dynamic programming based algorithm that is used to align the protein or DNA sequences. But the main limitation is that it can only compute the global optimality. Besides, it consumes considerable amount of memory and exponential time complexity is O(nm) where, n and m is the length of two sequence[10][11].

We also examined the Smith-Waterman [3] algorithm which can compute local alignment perfectly. But it can’t perform global alignment. Time & space complexity same as Needleman-Wunsch. T-coffee[4] proposed a new dynamic algorithm that is used to align the sequence. But the time complexity of T-coffee is exponential[9] such as $O(N^5L)$, where N is the number of sequences and L is the average sequence length. ProbCons[5] proposed a posterior probability based scoring method for all sub-optimal alignment. It also takes exponential time such as $O(k^2n^2 + k^3)time$. Newberg [6] proposed a memory efficient method which is used dynamic programming technique for calculating the index of the optimal check point. But It also takes exponential time complexity of $O(MN^3)$ or $O(N^4)$ and memory complexity of $O(N^2M)$, where M is the no. of states and N is the no query sequences. RSAM [7] and another algorithm [15] are also proposed a dynamic programming based algorithm which can solve the local sequence alignment problem. It also takes a considerable amount of time.

Our proposed algorithm deals with some specific types of problem. These types of problem scenarios are discussed according to following way: Firstly, In bio-sequence analysis, In many cases, the input or source sequence length is very long which contains billions of base pairs. On the other hand, the target sequence length is so short where the number of
base pair is not greater than 50. For this type of situation, we badly needed to divide or break the source or input sequence into the preference of the target sequence for further analysis such as aligning, matching or finding maximum matched sequence. So the first part of our algorithm is Fast Splitting(FS). FS breaks the huge sized input sequence into a feasible length according to the preference of the target. FS produces the Target Length Splitted Sequence (TLSS).

The second part of our proposed algorithm is Fast_MMSS Finder. In this part we take the TLSS and target sequence as input and find out the maximum matches sequence between each TLSS and target sequence. Then store the all maximum matched-sequence between every TLSS and target sequence. Sequence of alignment whole work we have various subsection such as system architecture, analytical representation, Complexity Analysis, Experimental set up, Experimental Evaluation.

2. METHODOLOGY
2.1 System Architecture
The system architecture of our proposed algorithm are consist with four layer. The integrated architecture started from input to the systems and stopped at finding Desired subsequence. Input Sequences may be any DNA, RNA and proteins. We have imposed our system for DNA data shows in Fig.1: ‘Fast_Splitter’ is used to split the input sequence into desired size,’Splitted Sequence store’ stores the output of Fast_Splitter which is Target Length Splitted Sequence(TLSS). ‘Fast_MMSS Finder’ is used to detect the matching point between TLSS & T. ‘Aligned sequence store’ is finally stored the desired result. Our initial input is two sequences. These are: Input or Source Sequence (S) and Target or Reference Sequence(T).

2.2 Fast Splitting(FS) Procedure
Algorithm 1: Fast Splitting(FS)
Input: Input Sequence(S) and Target Sequence(T).
Output: Target TLSS.

2.2.1 Fast_Splitting(Sequence_array,Start,End,M id,Target_TLSS)
1: Sequence_array ← AAA...TTT
2: Last ← length of (Sequence_array)
3: Start ← Sequence_array[0]
4: End ← Sequence_array[Last]
5: Mid ← int((Start+End)/2)
6: Tar_len ← Length of (Target_Sequence)
7: While Start<End do
8: Left_Recursor(Sequence_array,Start,M id)
9: Right_Recursor(Sequence_array,M id+1,End)
10: If(Total_dist(|Start-M id|)>Tar_len or Total_dist(|End-M id|) > Tar_len) then
11: get TLSS←TLSS with desired length.
12: End While.

Due to recursive subdivision, we reduce the data size. The complete flow chart is:

![Flowchart of Fast Splitting](image)

Fig. 1. : Complete Flowchart of Fast Splitting
Let’s see the successive subdivision for a sample sequence.

**Input Sequence**

| A | G | C | C | G | A | T | T | C | G | A | G | A | A | G | C | C | A | A | C | C |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|

*1st iteration*

Left Recursion

| A | G | C | C | G | A | T | T | C | G | A | G | A | A | G | C | C | A | A | C | C |

Right Recursion

| G | A | A | A | G | C | C | C | A | A | C | C |

*2nd iteration*

Left Recursion

| A | G | C | C | G | A | A | C | G | A | G | A | A | G | C | C | A | A | C | C |

Right Recursion

| G | A | A | A | G | C | C | C | A | A | C | C |

*nth iteration*

TLSS 1

TLSS 2

TLSS 3

TLSS

**2.3 Fast_MMSS**

Suppose \( X = (x_1, x_2, \ldots, x_n) \), \( Y = (y_1, y_2, \ldots, y_m) \) is the two bio-sequences as well as two TLSS from the Quick splitter, where \( x_i, y_i \in \{A,C,G,T\} \). We can denote an array \( CA \) of the four characters so that \( CA(1) = "A" \), \( CA(2) = "C" \), \( CA(3) = "G" \) and \( CA(4) = "T" \). To find Maximum Matches Sub-sequence between TLSS and \( T \), we firstly construct the tables of successors of the uniform characters for the two strings. The successor tables of \( X \) and \( Y \) are defined as \( GX \) and \( GY \).
Definition 1: [8]
For the sequence $X = (x_1, x_2 \ldots x_n)$, its successor table $SX$ of identical character is defined as:

$$GX(i, j) = \begin{cases} \min \{k | k \in SX(i, j) \}, & SX(i, j) \neq \emptyset \\ - & \text{Otherwise} \end{cases}$$

Here, $SX(i, j) = \{k | x_k = CA(i), k \geq j\}, i = 1,2,3,4, j = 0,1, \ldots n$. If $GX(i, j)$ is not “-”, it denotes that the index of the next character similar to $CA(i)$ after the $j$th index in sequence $X$. If $GX(i, j)$ is equal to “-”, it denotes that there is no character $CA(i)$ after the $j$th index.

Example 1: [8]
Let $X = "G C T A T A ".$ The corresponding successor tables of $GX$ is shown

| i | CA(i) | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|---|-------|---|---|---|---|---|---|---|
| 1 | A     | 4 | 4 | 4 | 4 | 6 | 6 | - |
| 2 | C     | 2 | 2 | 2 | - | - | - | - |
| 3 | G     | 1 | - | - | - | - | - | - |
| 4 | T     | 3 | 3 | 3 | 5 | 5 | - | - |

Lemma 1[8]. We denoted the length of the maximum matches subsequence of $X, Y$ as $|MMSS(X, Y)|$, then $|MMSS(X, Y)| = \max (\text{level } (i, j) \{ (i, j)^5S(X, Y) \}$.

Algorithm Fast_MMSS
Input: An array of string which contains the TLSS from Fast_Splitter (algo. 1) in each index and the Target Sequence.
Output: Perfectly aligned sequence with desired accuracy.
1: Array[N]\text{=\{TLSS}_1, TLSS_2, \ldots \ldots \ldots \ldots \ldots TLSS_n\}}$
Where, $N$ is the no. of TLSS from Fast_Splitter.
Store[N] is an empty array which contain the final output.
2: Store[N] = \emptyset
3: for init = 0 to N do
For each Array[i] Call Procedure 1;
4: Store[i] \leftarrow \text{Output of Procedure 1 for Array[i]}$
5: \text{End for.}

Procedure 1[8]:
Input: Target Sequence and Array[i] where $i$ means ith TLSS.
Output: Perfectly aligned sequence for Array[i].
Begin:
1: Firstly make the tables $GX$ and $GY$;
2: Search for all the initial uniform character pairs:
   $(GX(k, 0), \text{GY}(k, 0)), k = 1, 2, 3, 4$;
3: Then put all the initial uniform pairs $(k, \text{GX}(k, 0), \text{GY}(k, 0), 0, \emptyset, \text{action})$, $k = 1, 2, 3, 4$ to the table pairs.
Put this value. For all the initial uniform pairs,

$\text{pos}=1, \text{prev}=\emptyset$ and state=$\text{action}$

4: Repeat
5: for all action uniform pairs $(k, i, j, \text{pos}, \text{prev}, \text{action})$ in pairs parallel-

Do Generate all the successors of $(k, i, j, \text{pos}, \text{prev}, \text{action})$.

Shift the state of $(k, i, j, \text{pos}, \text{prev}, \text{action})$ into inaction.
End for
6: Until any record found in action state in table pairs.
7: Calculate $z =$ the maximal level in the table pairs.
8: For all uniform pairs $(k, i, j, z, l, \text{inaction})$ with $\text{pos} = z$ in pairs
Parallel do
Pradi = l; Res(z) = $x_z$
While Pradi $\neq \emptyset$ do
8.1.1: take the Pradi-th record (prev, g, h, z', l', \text{inactive}) from table pairs.
8.1.2: Pradi = l'; Res(z') = $x_{z'}$
8.3: End While.
End.

3. EXPERIMENTAL RESULT & COMPLEXITY ANALYSIS
3.1 Efficiency of the System
Let time required by random data set as Random time is = $T_r$
Time required by quick splitting process is = $T_s$
Total integrated time for all data set time is = $T_i$
Overhead time or non-useful time is = $T_r-T_s$ (Due to random timing)
Total time spent for all DNA segments are $T_i = \theta n \cdot T_s$
Here,
$n =$ Number of segments of DNA.
So we can define speedup is the ratio between random time dataset processing to Bounding box bounded time

$$\text{Speed Up} = \frac{\text{Random Time}}{\text{Quick Splitting Time}} \cdot \frac{T_s}{T_r}$$

By using the mathematical equations, we can define as $T_r = \theta (n^3)$ due to its randomness.

$T_s = \theta (n\log n)$

So the speed up is

$$\text{Speed up} = \frac{\theta(n)}{\theta(n\log n)}$$

Example:
For the data length $n = 4$
The serial time for linear is 256 ns seconds.
The quick splitting time is 2.41 ns.
The speedup would appear = 256/2.41 = 106.22ns
Efficiency is a measure of the fraction of time for which a processing element is usefully employed. Mathematically, it is given by
\[ E = \frac{s}{p} \]
Following the bounds on speedup, efficiency can be as low as 0 and as high as 1.

3.2 Implementation tools
Firstly, we needed to set Cygwin environment on our system. On that purpose, we preferred the latest version of Windows 10 Enterprise. Finishing the installation of the environment it is required to install the proper libraries for running the experiment. Then C++11, GNU GCC, OpenMPI libraries are installed with proper manuals and instructions. Code::Blocks IDE and Sublime Text Editor is being installed for code generation, modifications and experimental purposes.

3.3 Experimental Result
CPU utilization time & Execution time comparison with different algorithm is (see Fig. 4 & Fig. 5).

Fig. 4 & Fig. 5 illustrates the execution time & CPU utilization time for sequence alignment for different data length. The bar chart indicates the CPU utilization time for sequence alignment. The skyblue bar indicates CPU utilization for QS+Fast_MMSS. Orange and ass bars are indicates the CPU time for RSRM and BLAST respectively. Less DNA sequence need less CPU time. Our QS+Fast_MMSS measures less CPU. QS+Fast_MMSS used divide and conquer approach for data splitting and reduced the data size. Though, MMSS finding approach performs in linearly. But MMSS finding process has less effect in CPU utilization. RSRM measures less CPU time than BLAST and maximum than QS+Fast_MMSS. RSRM used bounding box approach for data splitting. Bounding box approach selects the data from large data sets in linearly. It also randomly selects the data pattern that need more time than our divide and conquer approach.

| Data Length | QS+Fast_MMSS(s) | RSRM(s) | BLAST(s) |
|-------------|-----------------|---------|----------|
| 1000000 bp  | 0.35            | 0.39    | 0.47     |
| 1500000 bp  | 0.37            | 0.41    | 0.49     |
| 2000000 bp  | 0.40            | 0.43    | 0.52     |
| 2500000 bp  | 0.42            | 0.45    | 0.53     |
| 3000000 bp  | 0.43            | 0.46    | 0.55     |
| 3500000 bp  | 0.45            | 0.48    | 0.56     |
| 4000000 bp  | 0.46            | 0.50    | 0.58     |
| 4500000 bp  | 0.50            | 0.53    | 0.60     |
| 5000000 bp  | 0.51            | 0.55    | 0.63     |
| 5500000 bp  | 0.53            | 0.56    | 0.66     |
| 6000000 bp  | 0.55            | 0.57    | 0.69     |
| 6500000 bp  | 0.57            | 0.59    | 0.70     |
| 7000000 bp  | 0.59            | 0.60    | 0.71     |
| 7500000 bp  | 0.60            | 0.62    | 0.71     |
| 8000000 bp  | 0.61            | 0.64    | 0.73     |

Fig 6: Visualization CPU utilization time comparison with different algorithm
3.4 Complexity
Our main focus is on time complexity. For computing the time complexity, we should consider the following parameters:

- Total number of dataset = N
- Length of the given data set = n
- Number of segments = t

- Random Search Time = T_r
- Splitting Time = T_s

**Complexity of FS:**
In all cases: $T(n) = 2T\left(\frac{n}{2}\right) + \alpha n$

\[
= 2 \left( 2T\left(\frac{n}{4}\right) + \frac{\alpha n}{2} \right) + \alpha n \\
= 2^2T\left(\frac{n}{4}\right) + 2\alpha n \\
= 2^\log_2\frac{n}{4}T\left(\frac{n}{4}\right) + 3\alpha n \\
= 2^kT\left(\frac{n}{4^k}\right) + k \propto n \\
T(n) = nT(1) + \alpha \log n, \text{ which is } O(n \log n).
\]

**Complexity of Fast_MMSS**
If we use the parallel implementation technique, then the time complexity of Fast MMSS is $O(n|\text{MMSS}(X,Y)|)$ in all cases[8], here $|\text{MMSS}(X,Y)|$ is the length of the MMSS of TLSS & Target sequence. Here, n is the total no. of TLSS. So the Overall Complexity is $= O(n \log n) + n|\text{MMSS}(X,Y)|$.

**Space Complexity**
Though our algorithm only focused about time efficiency, but our algorithm space-efficient also. We compare the memory requirement between Needleman-Wunsch [2], BLAST[1] and RSAM[7].

### Table 3. Comparison of Memory Complexity and Memory requirement between Needleman-Wunsch, BLAST and our proposed algorithm

| Algorithm       | Complexity       | Memory requirement          |
|-----------------|------------------|-----------------------------|
| Needleman-Wunsch | $O(M \times N)$  | $(M \times N)$              |
| BLAST           | $O(w \times (m+n))$ | $(m+n+(w \times (m+n)))$   |
| FS+Fast_MMSS    | $O(m+n+4^*(n+1)+4^*(m+1))$ | $m+n+4^*(n+m+2)$            |

4. CONCLUSION
In the paper, we have proposed a time efficient DNA sequence analysis algorithm, called FS+Fast_MMSS that can manage the huge dataset dynamically. FS+Fast_MMSS require very less time than that of BLAST or other previous algorithm. Experiment results prove the effectiveness of our proposed algorithm. We have worked with experimental dataset. Further, this concept will be implemented for real world dataset, RNA & Protein sequences and also use this concept to handle the dislocated or broken sequences.

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