Feedback determines the structure of correlated variability in primary visual cortex

Adrian G. Bondy 1,2,*, Ralf M. Haefner 3 and Bruce G. Cumming 1

The variable responses of sensory neurons tend to be weakly correlated (spike-count correlation, \( r_{sc} \)). This is widely thought to reflect noise in shared afferents, in which case \( r_{sc} \) can limit the reliability of sensory coding. However, it could also be due to feedback from higher-order brain regions. Currently, the relative contributions of these sources are unknown. We addressed this by recording from populations of V1 neurons in macaques performing different discrimination tasks involving the same visual input. We found that the structure of \( r_{sc} \) (the way \( r_{sc} \) varied with neuronal stimulus preference) changed systematically with task instruction. Therefore, even at the earliest stage in the cortical visual hierarchy, \( r_{sc} \) structure during task performance primarily reflects feedback dynamics. Consequently, previous proposals for how \( r_{sc} \) constrains sensory processing need not apply. Furthermore, we show that correlations between the activity of single neurons and choice depend on feedback engaged by the task.

Judgments made about sensory events (i.e., perceptual decisions) rely on the spiking discharge of sensory neurons. For this reason, there has been longstanding interest in the observation that this discharge tends to be variable given a fixed stimulus. In principle, this variability could confound perceptual judgments, impairing the fidelity of sensory information in the brain. Even worse, this variability tends to be weakly correlated amongst sensory neurons (spike-count correlation, \( r_{sc} \)), meaning it cannot trivially be averaged away. For this reason, \( r_{sc} \) is widely referred to as "correlated noise".

This way of thinking has underlain several influential lines of research in systems neuroscience. One has sought to understand the magnitude of the perceptual impairment introduced by \( r_{sc} \) in different behavioral contexts. When \( r_{sc} \) is distributed such that correlated fluctuations mimic the sensory events being detected or discriminated, it could severely impair perceptual accuracy. A related line of research has sought to understand how correlated variability affects the choices subjects make in perceptual discrimination tasks from trial to trial. These studies have shown that \( r_{sc} \) structure can give rise to a weak correlation between variability in single neurons and perceptual reports (choice probability; CP), consistent with the notion that CP observed in real neurons reflects the causal influence of correlated sensory neuronal variability on perception.

However, we currently know very little about the origin of \( r_{sc} \), making it unclear to what degree these conclusions are correct. A frequent (although typically unstated) assumption is that \( r_{sc} \) in sensory neurons is generated by shared variability in common afferent inputs. Consistent with this idea, \( r_{sc} \) correlates with the physical proximity and similarity in stimulus preference of neuronal pairs, which are also predictive of the degree of feedforward input convergence. If this explanation is correct, it supports the traditional view of \( r_{sc} \) as "confounding noise," as it arises from stochastic processes in the sensory encoding pathway. However, the bulk of synaptic inputs to sensory cortical neurons are not strictly feedforward in nature. Consequently, variation over time in shared inputs from downstream areas (i.e., top-down or feedback) may make a substantial contribution to \( r_{sc} \). These signals may reflect endogenous processes like attention, arousal or perceptual state and could be under voluntary control. In principle, this source of correlated variability need not confound perceptual judgments, but instead may reflect ongoing neuronal computations.

Several recent studies have shown that \( r_{sc} \) does change to some degree with task context, suggesting a top-down component. These studies have shown that \( r_{sc} \) in populations of sensory neurons can either increase or decrease depending on attentional state or other task demands. However, prior studies have made only limited measures of \( r_{sc} \) structure and how this changes with task, yet these are critical for understanding how \( r_{sc} \) arises and how it relates to task performance. Furthermore, the relative magnitude of feedforward versus top-down contributions to \( r_{sc} \) has not been determined. It also unknown whether task-dependent changes in \( r_{sc} \) reflect an adaptive reduction of sensory noise or whether \( r_{sc} \) is, in the first instance, generated by variability over time in top-down inputs reflecting downstream computations.

In the present study, we used large-scale neuronal population recordings in behaving macaques, along with careful behavioral control and an innovative analytical approach, to substantially advance our understanding of these fundamental questions. Subjects performed a variety of orientation-discrimination tasks using the same set of stimuli. The only difference between tasks was the set of orientations being discriminated. If \( r_{sc} \) primarily reflects noisy sensory encoding, it should be invariant to changes in the task, given fixed retinal input. Alternatively, if it changes dynamically with the task, this would indicate that it reflects top-down signals. This experimental approach, inspired by a previous study, was combined with large-scale population recordings, allowing us to estimate the full \( r_{sc} \) matrix—that is, how \( r_{sc} \) varies as a function of all possible combinations of pairwise orientation preference. This made it possible to directly infer which components were fixed and which changed with the task. Strikingly, we could not identify a component that remained fixed. Instead we observed a pattern of task-dependent changes that was highly systematic and could be modeled as the effect of a single modulatory input targeting the two

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1Laboratory of Sensorimotor Research, National Eye Institute, NIH, Bethesda, MD, USA. 2Brown-NIH Neuroscience Graduate Partnership Program, Providence, RI, USA. 3Brain & Cognitive Sciences, Center for Visual Science, University of Rochester, Rochester, NY, USA. *e-mail: adrian.bondy@gmail.com
task-relevant subpopulations of V1 neurons in an alternating fashion across trials.

These data give unprecedented insight into the functional role of \( r_w \) structure in task performance. First, they show that the task-dependent changes in \( r_w \) structure appear to degrade the task performance of an ideal observer of V1 activity alone, because they mimic task-relevant stimulus changes. However, our discovery of the feedback origin of these correlations means that they need not degrade performance and points to the possibility that they may instead be a signature of ongoing neuronal computations. Indeed, recent circuit models of perceptual inference predict feedback signals whose statistics reflect the subject’s prior beliefs about the task, yielding predictions that closely match our observations\(^{28,29}\). Second, we show quantitatively that these feedback dynamics are the primary source of the choice-related activity we observed in V1, clarifying an ongoing debate\(^{30,31}\) about the interpretation of choice-related signals in sensory neurons. We conclude that \( r_w \) in sensory neurons reveals less than previously thought about the encoding of sensory information in the brain, but potentially much more about the interareal computations underlying sensory processing.

**Results**

We trained two rhesus monkeys (Macaca mulatta) to perform a two-alternative forced-choice coarse orientation-discrimination task (Fig. 1), used previously\(^{31}\). On a given trial, the subject was shown a dynamic, two-dimensional filtered noise stimulus for 2 s, after which it reported the stimulus orientation by making a saccade to one of two choice targets (oriented Gabor patches). Different task contexts were defined by the pair of discriminandum orientations. The stimuli were bandpass filtered in the Fourier domain to include only orientations within a predetermined range. The stimulus filter was centered on one of the two task orientations and its orientation bandwidth was used to control task difficulty. We included 0% signal trials, in which the stimuli were unfiltered for orientation (and thus the same regardless of context), to examine the effect of task context on \( r_w \) in the presence of a fixed retinal input.

To detect any effect of task context on \( r_w \) structure, it is critical that subjects based their choices on the presence of the correct orientation signals. To ensure this, we used psychophysical reverse correlation\(^{11–13}\) to directly measure the influence of different stimulus orientations on the subject’s choices (the ‘psychophysical kernel’). We found that subjects required multiple days of retraining after a change in the task context to fully update their psychophysical kernel. For this reason, we kept the task context fixed for the duration of each recording session and only undertook recordings in a new task context after subjects had updated their kernel (Supplementary Fig. 1). This is a noteworthy advance over past studies of the effect of task context on neuronal responses, which typically have not quantified the extent to which behavioral strategy truly matches task instruction.

We recorded spiking activity in populations of single V1 neurons using multielectrode arrays while the subjects performed the task. We determined the preferred orientation of each neuron by measuring its response to oriented stimuli (see Methods) in separate

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Fig. 1 | Orthogonal orientation discrimination task. a. Schematic illustration of the task. Two example task contexts shown (cardinal and oblique discriminations). The task context was fixed in a given recording session, but varied across sessions. b. Psychometric function for monkey LEM; example session M232, \( n = 1,354 \) trials. Black curve is a probit fit, and error bars are 95% confidence intervals around the mean (black points). c. Histograms showing the distributions of psychometric thresholds across sessions for the two subjects. Threshold is defined as the signal level eliciting 75% correct performance. Black triangle indicates the threshold corresponding to the example session in b. d. Example single stimulus frames corresponding to the two example task contexts in a. The stimuli consisted of dynamic white noise, filtered in the Fourier domain for orientation (see Methods). The filter was centered on one of the two task orientations and its bandwidth determined signal strength.
Fig. 2 | \( r_{sc} \) structure in V1 depends systematically on task context.

**a,** c. Observed \( r_{sc} \) matrices for two subsets of sessions grouped by task context, as indicated in **b.** The matrices were obtained by pooling the set of \( r_{sc} \) measurements made within each subset and applying a von Mises smoothing kernel (approximating a two-dimensional wrapped Gaussian with 15° s.d.). Colored dots correspond to pairs preferring the same or opposing task orientations. **b,** Polar histogram shows the distribution of task contexts used across sessions, with color indicating the division into two subsets. Note that the period is 90° because of the orthogonality of the discriminanda. Colored arrows indicate the mean task context associated with each subset. **d,** Scatter plot showing a weak, but significant, dependence of \( r_{sc} \) on the difference in preferred orientation of neuronal pairs (Pearson’s \( r = -0.11 \), \( P = 9 \times 10^{-4} \), bootstrap test, one-sided). Black line is a type II regression line and gray line corresponds to \( r_{sc} = 0 \). **e,** Average \( r_{sc} \) matrix observed across all sessions, shown in a task-aligned coordinate frame. Each pair’s preferred orientations are expressed relative to the task orientations. Mean \( r_{sc} \) values are close to 0 due to the inclusion of a model constant.

**R_{sc} structure changes systematically with task context.** Recording large populations gave us the power to measure the full \( r_{sc} \) matrix, that is, how \( r_{sc} \) varied as a function of all possible combinations of orientation preference. To our knowledge, this is the first time such detailed measures of \( r_{sc} \) structure have been made while animals perform a discrimination task. To assess the presence of task-dependent \( r_{sc} \) structure in the data, we first divided the recording sessions into two groups based on the task context used (Fig. 2b). We estimated the smoothed, average \( r_{sc} \) matrix associated with each subset (Fig. 2a,c) by pooling \( r_{sc} \) values measured across the subset of sessions, along with measures of the neuronal preferred orientation. Across both subsets of sessions, we observed a tendency toward higher values of \( r_{sc} \) for pairs of neurons with more similar orientation preferences (i.e., higher values closer to the diagonal of the matrix), consistent with numerous prior observations (Fig. 2d). Traditionally, such observations were presumed to reflect ‘limited-range correlations’ that depend only on similarity in stimulus preference, equivalent to a rotationally symmetric (Toeplitz) correlation matrix. In contrast, in our data this was due to distinct patterns in the two matrices: we observed the highest values of \( r_{sc} \) among pairs that shared a preferred orientation close to a discriminandum, and the lowest values of \( r_{sc} \) tended to occur amongst pairs preferring opposite task orientations. Because the task context differed between the two subsets, this yielded matrices with a lattice-like
Segregating fixed and task-dependent components of \( r_{sc} \) structure.

Our dataset of \( r_{sc} \) measurements, made in large, heterogeneous populations across diverse task contexts, allowed us to directly estimate the \( r_{sc} \) structure that was fixed versus the structure that was dynamically changing with task. To do this, we modeled the raw \( r_{sc} \) values using two structured components: (i) a fixed \( r_{sc} \) matrix describing the dependence of \( r_{sc} \) on pairwise orientation preference regardless of task and (ii) a task-dependent \( r_{sc} \) matrix capturing the dependence of \( r_{sc} \) on pairwise orientation preference relative to the task orientations. We used ridge regression to find the form of these two component matrices that best predicted the raw \( r_{sc} \) measurements. To reduce the number of regressors without constraining the form of these two components, we parameterized the matrices as 8 × 8 grids of basis functions (Fig. 3a and see Methods).

This modeling approach allowed us to address two related questions. First, the form of the fitted components serves to identify the nature of the dynamic and fixed \( r_{sc} \) structure in the V1 population. Second, comparing models that included either or both components provided a quantitative test for the origin of the \( r_{sc} \) structure we observed. When we jointly fit both components to the data, the inferred task-dependent component (Fig. 3c) recapitulated the lattice-like structure we observed in the average data (Fig. 2e). The fixed component (Fig. 3d) was smaller in amplitude and, notably, appeared also to contain a weak lattice-like structure, offset by approximately 30°. This is likely due to the fact that we did not uniformly sample across all possible task contexts, with tasks discriminating orientations near 30° and 120° being overrepresented (Fig. 2b). Next, we compared reduced models in which only one of the two components was used. Strikingly, cross-validated model accuracy was increased when we removed the fixed component entirely, but reduced by about half when we removed the task-dependent component (Fig. 3b). This suggests that the dependence of \( r_{sc} \) on orientation preference in our data can be explained as a completely dynamic phenomenon, with no additional dependence that is invariant to the task. We found that all of these modeling results could be replicated when the fixed and task-dependent components were parameterized in a different way (using a variable number of basis functions with locations fit to the data, instead of a fixed grid of basis functions; Supplementary Fig. 8 and see Methods), suggesting that the conclusions do not depend on the particular parametric assumptions that were made.

Fig. 4 | \( R_{sc} \) structure during task performance reflects a single mode of variability. a, Eigenspectrum for the average, task-aligned \( r_{sc} \) matrix in Fig. 2e. The largest eigenvalue exceeded chance (**P < 0.001, permutation test, one-sided). The chance distribution (mean ± 1 s.e.m.; blue) was determined by adding a random offset to the preferred orientations of each of the 811 pairs (i.e., permuting each \( r_{sc} \) value along the diagonal). b, The eigenvector corresponding to the largest eigenvalue in a. We first removed the mean \( r_{sc} \) value from the matrices to ignore any flat eigenvectors. Error shading shows ±1 bootstrap s.e.m. The dark gray vertical bar indicates the peak in the eigenvector ±1 bootstrap s.e.m. This was not significantly different from 0° (P = 0.078, bootstrap test, one-sided), indicating close alignment with the task. c, Schematic of the single-eigenvector model, in which \( r_{sc} \) structure is described as the outer product of a vector parameterized as the difference between two von Mises functions 90° apart. d, Schematic of the diagonal-ridge model, in which \( r_{sc} \) structure depended only on the difference in preferred orientations, independent of task. This dependence was modeled as a von Mises function centered on zero. e, Goodness-of-fit for the models in c and d, calculated as normalized percent of variance explained, as in Fig. 3. Error bars around the mean and statistical comparison between models obtained through repeated 50-fold cross-validation of the set of 811 pairs.
We were interested in the effect of task context on $r_w$ structure, so it made sense to focus on the dependence of $r_w$ on orientation preference. However, $r_w$ depends on a large number of factors irrelevant to the present study, such as physical proximity between pairs and similarity in tuning along many stimulus dimensions apart from orientation. This implies that a model that describes the dependency on orientation preference correctly will only explain a small fraction of the variance in $r_w$. (This can be appreciated in Fig. 2d, f, where pairs with similar locations on the abscissa have substantial variation in $r_w$.) To estimate this fraction, we assessed the accuracy with which we could predict individual $r_w$ values from a smoothed matrix built with other pairs. This showed that, in principle, 3.6% of the variance is explainable, of which the majority was explained by the regression model above. We also found that, across cross-validation folds, the fitted model showed that, in principle, 3.6% of the variance is explainable, of which the majority was explained by the regression model above.

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**$R_w$ structure during task performance reflects a single mode of variability.** In the modeling discussed so far, we aimed to describe a fixed and task-dependent component of $r_w$ structure with as few assumptions as possible. Having established that the observed $r_w$ structure can be best described by assuming it is entirely task-dependent, we next sought to identify a more parsimonious and intuitive description of this task-dependency. We started with the observation that the pattern we observed—increased correlation between pairs preferring the same task orientation and decreased correlation for pairs preferring opposing task orientations—would be consistent with feature-selective feedback that varied in its allocation from trial to trial between the two task-relevant orientations, as has been shown in recent theoretical studies. To quantify this observation, we performed an eigendecomposition of the smoothed, average $r_w$ matrix (as in Fig. 2e), shown separately for each stimulus strength. Note that 0% signal trials involved statistically identical stimuli across all task contexts. A qualitatively similar structure was apparent at nonzero signal levels. Spike counts were z-scored to eliminate the effect of stimulus drive; see Methods. Scatter plot showing the slope of a regression line comparing the $r_w$ values measured at each signal level against the $r_w$ values measured at the 0% signal level. This quantity indicates the degree of attenuation of the $r_w$ structure at a given signal level. We observed a weak but significant negative correlation with signal strength (Pearson’s $r = 0.038$, bootstrap test, one-sided; error bars are ±1 bootstrap s.e.m. around the mean of the 811 pairs), implying that the $r_w$ structure is attenuated on high-signal trials, when there was also less variability in choice. Dotted line is fitted regression line.

**Fig. 5** | $R_w$ structure matches effect of task-related stimulus variability. **a.** Responses (mean ± 1 s.e.m.; $n = 1,049$ trials) to the stimuli used in the task at various signal strengths for two example neurons (G020.1, green; G020.12, blue) in monkey JBE. For the purposes of illustration, the two task orientations are simply labeled positive and negative. This pair was typical in that the response functions ($f_1$ and $f_2$) are approximately linear over the range of signal strengths used. For this reason, we calculated the response correlation introduced by tuning similarity as the normalized product of the derivatives $f_1 f_2^\prime$. **b.** The matrix of $f_1 f_2^\prime$ values, as a function of task-aligned pair orientation preference, was obtained using kernel smoothing, as in Fig. 2. We observed a pattern that was very similar to the structure of $r_w$ we observed during task performance (Fig. 2e). **c.** Scatter plot of the task-dependent (putatively top-down) component of $r_w$ (Fig. 3c) against normalized $f_1 f_2^\prime$ values for each recorded neuronal pair. The two were highly correlated across the population (Pearson’s $r = 0.61$, ***$P < 0.001$, bootstrap test, one-sided).
structure we observed in V1 could indeed be well described as the result of a single source of covariability that changed dynamically with the task.

We compared the single-eigenvector model with another simple model that more closely reflected standard assumptions about $r_{sc}$ structure in sensory brain areas. This model predicted that $r_{sc}$ would depend only on the difference in preferred orientation between pairs of neurons regardless of task ($r_{sc}$ limited-range correlations yielding an $r_{sc}$ matrix with a diagonal ridge) and would be consistent with $r_{sc}$ structure due to common afferent inputs. We modeled this dependence as a von Mises function of preferred orientation difference (Fig. 4d). This model performed much worse in predicting the observed set of $r_{sc}$ values, failing to exceed chance performance (Fig. 4e). (This qualitative difference in model performance was replicated in both subjects individually; see Supplementary Fig. 2.) Notably, both of these simple models predict a dependence of $r_{sc}$ on preferred orientation difference, similarly to what we found in the data (Fig. 2d) and to has been observed previously; however, in the case of the single-eigenvector model, this is due to task-dependent changes in $r_{sc}$ while for the diagonal-ridge model there is no effect of task context. Notably, we found that during the passive fixation blocks, the diagonal-ridge model performed better (Supplementary Fig. 3c), quantitatively supporting the observation that the task-dependent correlations we observed require active task engagement.

**Effect of task-dependent $r_{sc}$ structure on neural coding.** We next sought to address the functional importance of the $r_{sc}$ we observed on sensory coding. Many studies have shown that $r_{sc}$ in sensory neurons can decrease the sensory information that can be decoded, particularly when $r_{sc}$ resembles correlations due to task-related stimulus.
We estimated this task-related stimulus correlation as the product of the slopes of a pair’s mean response functions along the task axis (i.e., as a function of orientation signal strength; Fig. 5a)\(^6\), normalized by the product of the neuronal variances. When we plotted these values as a smooth, task-aligned matrix (Fig. 5b), we observed a lattice-like pattern strikingly similar to that in the observed \(r_w\) matrix (Fig. 2c). Confirming this similarity, the task-dependent component of \(r_w\) structure identified by the regression model was strongly correlated on a pair-by-pair basis with the stimulus-induced correlations (\(r=0.61\); Fig. 5c). This matches our earlier observation that \(r_w\) structure was consistent with feedback that alternatingly targeted the task-relevant neuronal pools, which is similar to the effect of varying the stimulus along the axis defining the task.

Thus, the observed \(r_w\) structure appears not to improve, but rather to degrade, the sensory representation. However, our results highlight a problem with this interpretation and any purely feedforward account of the functional role of \(r_w\). Namely, \(r_w\) that is generated endogenously need not be problematic at all (for example, if the decoder had access to those endogenous signals). Indeed, the propagation of feedback signals that are matched to the statistics of the relevant sensory stimuli may be an adaptive strategy for bringing prior knowledge to bear, as predicted by recent models of probabilistic perceptual inference\(^{15,16}\). \(r_w\) resembling stimulus-induced correlations emerges in such models\(^2\) as a consequence of the subject developing the appropriate priors about the task, yielding predictions that both match our empirical findings and offer a normative explanation.

**Relationship between \(r_w\) structure and perceptual choice.**

Correlations between trial-to-trial variability of single neurons and choice\(^-15\) have been frequently observed throughout sensory cortex. Theoretical studies have emphasized that this suggests the presence of spike-count correlation with a particular structure\(^-16\). After all, if many sensory neurons have variability that is correlated with choice, this implies that neurons supporting the same choice are themselves correlated. However, this could be compatible with either or both of two causal mechanisms: (i) correlated fluctuations directly affect the choices a subject makes to trial (a feedback-forward source of choice-related activity); or (ii) the correlated fluctuations reflect variation across trials in a feedback signal related to the upcoming choice (a feedback source). As we show, our detailed measures of \(r_w\) structure during task performance can address this ongoing debate.

First, we reasoned that evidence of feedback related to the upcoming choice would be an \(r_w\) structure in V1 whose magnitude depends systematically on variability in choice. Consistent with this prediction, we found that the amplitude of the \(r_w\) structure was attenuated on high-signal trials relative to 0% signal trials, in a manner that depended systematically on signal strength (Fig. 6a, b). However, this attenuation was modest, even at the highest signal level we analyzed (11% reduction), despite the highly uneven distribution of choices. This rules out the extreme scenario in which feedback perfectly reflects choice. Supporting this conclusion, we found that the \(r_w\) structure, when calculated using only spikes from different 200-ms windows during the trial, showed a stable time-course (after a precipitous drop at the first timepoint) and did not grow in amplitude with decision formation (Fig. 7). Taken together, these observations support the conclusion that \(r_w\) structure reflects variation in feedback signals only partially correlated with the subject’s final choices. These could include a combination of bias, attention to orientation, prior beliefs and/or a decision variable.

Next, we assumed standard feedforward pooling (i.e., linear readout weights applied to the sensory pool) to determine whether the observed \(r_w\) structure would be quantitatively consistent with the observed choice-related activity. To do this, we made use of recent theoretical work that analytically relates \(r_w\) structure, readout weights and choice-related activity\(^8\). We calculated CP, which quantifies the probability with which an ideal observer could correctly predict the subject’s choices using just that neuron’s responses\(^9,24\), for each recorded neuron. We found an average CP of 0.54 for task-relevant neurons, significantly above chance level (Fig. 8a) and similar in magnitude to that found by another study using the same task\(^2\). We found that the \(r_w\) structure we observed would be sufficient to produce a pattern of CP across the population consistent with the data (Fig. 8b,c), across a wide range of possible readout schemes (Supplementary Fig. 9). Next, we considered the contribution of the different inferred sources of \(r_w\) to CP. (For top-down sources of correlation, this is equivalent to assuming that the sensory population is read out without taking into account the top-down signal.) This allows us to treat all sources of \(r_w\) equivalently and compare them quantitatively. When we considered a population containing only the task-dependent component of \(r_w\) structure identified in the regression model (Fig. 3c), predicted CP was only slightly reduced. Assuming only the fixed component (Fig. 3d), however, drastically reduced predicted CP below what we observed (Fig. 8b, c). Thus, our data rule out the view that a substantial component of CP merely reflects the feedforward effect of stochastic noise in the afferent sensory pathway. Instead, the main source of CP appears to depend on task-dependent changes in \(r_w\) structure related to perceptual judgments.

**Discussion**

Spike-count correlations between sensory neurons have typically been described as reflecting noise that corrupts sensory encoding\(^1,15\). However, little is known about the origin of \(r_w\) and it may instead be due to changes over time in feedback signals. We addressed this by recording from populations of V1 neurons using multielectrode arrays while macaque subjects performed a set of orientation discrimination tasks. This approach allowed us to estimate the entire matrix describing the dependence of \(r_w\) on pairwise orientation preference (Fig. 2), providing an unprecedented clear picture of \(r_w\) structure in a behaving animal. By determining to what extent the \(r_w\) matrix was fixed and to what extent it changed with task, we inferred the relative importance of feedforward and feedback pathways in generating it (Fig. 3). We found systematic and novel structure in the \(r_w\) matrix that changed in a predictable manner with the task. Using multiple modeling approaches, we found that the fixed \(r_w\) structure was much smaller than the task-dependent structure, so much so that we could not estimate a fixed component reliably. Notably, a single source of task-dependent feedback captured the pattern we observed (Fig. 4). This feedback input increased and decreased the firing rate of neurons tuned for the two task-relevant orientations in a push–pull manner.

Our results suggest the possibility that variability in feedback is a major source of \(r_w\) structure in sensory cortex. The role of feedback may be even more pronounced in areas downstream of V1 that typically show a greater degree of extrasensory modulation\(^15,18–20\). At the same time, we cannot rule out a larger role of feedback inputs in generating patterns of \(r_w\) defined in different ways than those uncovered here. For example, because our measures of \(r_w\) structure involved smoothing, we cannot rule out the possibility that the fine-grained structure of \(r_w\) behaves in ways not captured by our analysis.

Our results are consistent with, and expand upon, those of a prior study that also measured task-dependent changes in \(r_w\)\(^27\). In that study, single pairs of direction-selective neurons from area MT were recorded while subjects performed two direction-discrimination tasks chosen by the experimenters to probe the effect of task context: one in which the neurons contributed to the same choice (‘same-pool’ condition) and one in which they contributed to opposite choices (‘opposite-pool’ condition). This amounts to a selective subsampling of the \(r_w\) structure. While this identified some degree
of task-dependence, the implications remained unclear. By contrast, the present study involved recordings from large, simultaneously recorded populations, which achieved much better coverage of the full r_{ne} structure. This revealed the detailed structure of the task-dependence and provided the basis for quantitative modeling and previously unpublished conclusions. For the purposes of comparison, we plotted our data in an analogous way to the prior study and found qualitatively similar results (Supplementary Fig. 10).

Consistent with several past studies, we found evidence for choice-related feedback, as shown by the finding that correlated fluctuations in V1 are more pronounced on trials where the subject's choices were more variable (Fig. 6). However, this effect was relatively weak, and we observed that task-dependent r_{ne} structure did not grow in amplitude with decision formation (Fig. 7), suggesting that processes indirectly related to choice may be responsible for the feedback generating the correlations. More importantly, we found that the standard assumption—that correlated fluctuations influence choice through feedforward pathways—predicted CP values in the V1 population that matched the data (Fig. 8), the first empirical test of the theoretical relationship between r_{ne} in sensory neurons, CP and readout. However, the r_{ne} structure responsible changed with the task, demonstrating that it does not simply reflect afferent noise. Taken together, our results instead favor the notion that choice-related activity comes about through self-reinforcing loops of reciprocal connectivity between cortical areas, as has also been suggested by other studies.

The task-dependent modulation of r_{ne} we observed did not appear to be beneficial to task performance (Fig. 5), at least not in the manner this has typically been examined (i.e., feedforward decoding of the sensory population alone). Instead, the inferred feedback signals appeared to mimic task-relevant stimulus changes, confounding the choices of an observer using only the sensory population. However, because the correlations reflect downstream computations, they need not be limiting in this way to the subject. Thus our results highlight the fundamental insufficiency of considering the theoretical implications of r_{ne} in terms of purely feedforward frameworks, as almost all such studies have done to date.

The inferred source of task-dependent feedback resembles previous reports about the effects of feature-based attention on visual cortical neurons. Feature-based attention enhances the firing rate of neurons tuned for the attended stimulus feature and decreases the firing rate of neurons tuned for unattended stimulus features. One possibility is that our task engages feature-based attention, which varies over time in its allocation between the two task-relevant orientations. This does not appear to provide an adaptive increase in the amount of relevant stimulus information encoded, contrary to traditional descriptions of attention.

However, as discussed above, once a top-down contribution to correlations is recognized, it is not possible to infer the amount of sensory information available to a decoder from the activity of a population of sensory neurons alone.

Our findings thus emphasize the need for new normative models that predict context-dependent feedback during perceptual processing. Currently, models based on hierarchical probabilistic inference do predict such feedback signals and account for many of our experimental findings. This work builds on the longstanding idea that the goal of a perceptual system is to generate valid inferences about the structure of the outside world, rather than to faithfully represent sensory input. This requires combining sensory input with prior beliefs, both of which can introduce correlated variability. During perceptual decision making, correlations resembling those induced by the stimulus naturally emerge as a consequence of the subject acquiring the appropriate prior beliefs about the structure of the sensory environment. Clearly, further development of this and other models of perceptual processing are needed to generate quantitative predictions that can be further tested empirically.

Methods
Methods, including statements of data availability and any associated accession codes and references, are available at https://doi.org/10.1038/s41593-018-0089-1.

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**Author contributions**

A.G.B. and B.G.C. conceived and designed the experiments. A.G.B. performed the experiments and all aspects of the analysis. A.G.B. and B.G.C. wrote the paper. R.M.H. advised and assisted with the data analysis and the paper. B.G.C. advised at all stages.

**Competing interests**

The authors declare no competing interests.

**Additional information**

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Correspondence and requests for materials should be addressed to A.G.B.

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Methods

Electrophysiology. We recorded extracellular spiking activity from populations of V1 neurons in two male, awake, head-fixed rhesus monkeys (Macaca mulatta), LEM and JBE. For the majority of the recordings, LEM was 14 while JBE was 16 years old, before which time they had each received extensive behavioral training, including on other behavioral experiments for LEM. LEM could not be pair-housed due to antisocial behavior. Both monkeys were implanted with a head post and scleral search coils under general anesthesia. In LEM, a recording chamber was implanted over a craniootomy above the right occipital operculum, as described previously, by which we introduced linear microelectrode arrays (U- and V-probes, Plexon; 24 contacts, 50- or 60-μm spacing) at an angle approximately perpendicular to the cortical surface with a custom microdrive. We positioned the linear arrays so that we roughly spanned the cortical sheet, as confirmed with current-source density analysis, and removed them after each recording session. In JBE, a planar Utah array (Blackrock Microsystems; 96 electrodes, 1 mm in mm in diameter); a task was targeted to target (U- and V-probe, layers, 400-μm spacing) was chronically implanted, also over the right occipital operculum. All procedures were performed in accordance with the US Public Health Service Policy on the humane care and use of laboratory animals, and all protocols were approved by the National Eye Institute Animal Care and Use Committee.

Broadband signals were digitized at 30 or 40 kHz and stored to disk. Spike sorting was performed offline using custom software in Matlab.

Visual stimuli. All stimuli were presented binocularly on two gamma-corrected cathode ray tube (CRT) monitors viewed through a mirror haploscope, at 85 or 100 Hz. The monitors subtended 24.1° x 19.5° of visual angle (1,280 x 1,024 pixels). The stimuli presented during the performance of the discrimination task consisted of bandpass-filtered dynamic white noise, as described previously. Briefly, stimuli were filtered in the Fourier domain with a polar-separable Gaussian. The peak spatial frequency was optimized for the recorded neuronal population (1 and 4 cpd pixels for LEM and JBE, respectively), while the peak orientation could take one of two orthogonal values the animal had to discriminate in a given session. The angular s.d. of the filter modulated the orientation bandwidth and was varied from trial to trial. A 2D Gaussian contrast envelope was applied to the stimulus so that its spatial extent was as small as possible while still covering the minimum response fields of the neuronal populations being recorded. The median envelope s.d. was 0.6° for both animals. The median stimulus eccentricity was 5.4° for LEM and 5.0° for JBE. In Fig. 1, we quantify orientation bandwidth as percent of signal strength. This was calculated as 100 x R, where R is the length of the resultant vector associated with the angular component of the stimulus filter. To perform psychophysical reverse correlation (PRC) for orientation (Supplementary Fig. 1), we determined the orientation energy of the stimulus on each trial as the radial sum of its 2D amplitude spectrum (averaged across frames) to remove information about spatial frequency and phase.

We estimated neuronal orientation preferences in separate blocks of trials, using 420-ms presentations of the following types of stimuli, presented at a range of orientations: (i) an orientation narrowband version of the stimulus described above (10° angular s.d.); (ii) sinusoidal gratings; and (iii) circular patches of dynamic random dot patterns. We targeted orientation bandwidths as percent of signal strength. This was calculated as 100 x R, where R is the length of the resultant vector associated with the angular component of the stimulus filter. To perform psychophysical reverse correlation (PRC) for orientation (Supplementary Fig. 1), we determined the orientation energy of the stimulus on each trial as the radial sum of its 2D amplitude spectrum (averaged across frames) to remove information about spatial frequency and phase.

Orthogonal orientation discrimination task. The animals performed a coarse orientation-discrimination task using the orientation-filtered noise stimuli, as described previously. To initiate a trial, the subject had to acquire a central fixation square. After a delay of 50 ms, the stimulus appeared for a fixed duration of 2 s. The trial was aborted if the subject broke fixation at any point during the stimulus presentation, defined as either (i) making a microsaccade covering a distance greater than a predefined threshold (typically 0.5°) or (ii) a deviation in mean eye position from the center of the fixation point of more than a predefined threshold, typically 0.7°. At the end of the stimulus presentation, two choice targets appeared. These were Gabor patches of 2-3° in spatial extent, oriented at each of the two task orientations. The locations of the choice targets depended on the task. For orientation pairs near horizontal and vertical (-22.5° to +22.5° and 67.5° to 112.5°), the choice targets were positioned along the vertical meridian, at an eccentricity of 30°, with the two tone vats oriented target always appearing in the upper hemifield. For orientation pairs near the obliques (22.5°-67.5° and 112.5°-157.5°), the choice targets were positioned along the horizontal meridian, at the same range of eccentricities, with the smaller of the two orientations always appearing in the left hemifield. (We use the convention that horizontal is 0° and that orientation increases with clockwise rotation.) To penalize random guessing, the animals performed a liquid reward delivery task after correct choices on each of the two trial sequences, abolishing stimulus-independent covariability, while preserving the identity between the stimuli associated with the two trial sequences.

We attempted to use as wide a range of task contexts as possible over the course of data collection from both animals, but task contexts were not presented in a random order. To perform a new task context, subjects were retrained for a few days at each time. Additionally, data collection and analysis was not performed blind to the experimental conditions—in particular, experimenters were aware of the instructed task context.

Spike-count correlation measurements. Spike-count correlations were calculated as the Pearson correlation between spike counts, counted over the entire duration of the stimulus, with a 50-ms delay to account for the typical V1 response latency. Spike counts were first z-scored separately within each experimental block (typically a set of 100–200 trials lasting about 10 min) and each stimulus condition. This removed correlations related to long-term firing rate nonstationarities and allowed us to combine trials at different signal levels without introducing correlations related to similarity in stimulus preference. We used a balanced z-scoring method proposed recently to prevent bias related to differences in choice distributions across signal levels. We excluded pairs that were not simultaneously isolated for at least 25 trials total. The median number of trials per pair during task performance was 752.

To control for the use of z-scoring, any influence of stimulus history on firing rates could, in principle, introduce a source of covariability that depended on the task context, since the set of stimuli used was not identical across task contexts (only the 0% signal condition was identical). We ruled out this confound by adapting the z-scoring procedure described above to further remove any information about the preceding stimulus contained in the spike rate on the current trial. To do this, we z-scored spike counts for each trial conditioned on all trials for which the current stimulus and the stimulus on the preceding trial were the same. This produced identical results to those shown in the main analysis (Supplementary Fig. 5).

A main goal of the study was to measure how spike-count correlation varies with pairwise orientation. We illustrate this dependence in several figures as a smoothed function estimated from measures of rsc combined across multiple recording sessions, which we then sampled discretely with 1° resolution. The smoothed estimates were obtained using a bivariate von Mises smoothing kernel. A point in the correlation matrix C was given as:

$$C(x, y) = \sum_{i=1}^{m} \sum_{\phi} \mathbb{K}(x, \theta_i, \phi) \mathbb{K}(x, \theta_i, \phi)$$

where $\theta_i$ is the orientation of the stimulus on the current trial, $\phi$ is the von Mises width parameter. We set $\kappa = 1.3t$, yielding a smoothing kernel closely approximating a bivariate wrapped Gaussian with 15° s.d. (Note that this smoothing procedure was only performed to generate figures in the manuscript and was not applied as a preprocessing step in any of the quantitative analyses.) In some cases, we expressed the $r_{sc}$ matrix in a task-centered coordinate frame (for example, Fig. 2c), for which the preferred orientations of the rth pair relative to the task orientations were used for $\theta_i$ and $\phi$. Since there were always two orthogonal task orientations, we averaged across both possible alignments, such that $C(x, y)$ = $C_{x+y 90°}$, $y + 90°$). All angular quantities were doubled for the calculations, as orientation has a period of 180°.

$\mathbb{K}(x, \theta, \phi) = \Theta(x, \theta, \phi)$

$\Theta(x, \theta, \phi) = \frac{1}{2\pi I_0(\kappa)} \int_0^{2\pi} \left(1 - e^{-\frac{\kappa^2}{2}} \cos(\phi) e^{-\kappa^{-2}} \cos((x - \theta) - \phi)\right) d\phi$

where $\Theta$ is the length of the Bessel function closely approximating a bivariate wrapped Gaussian kernel.
To generate the kernel-smoothed profile of CP (Fig. 8), we used a one-dimensional equivalent of the procedure above, in which preferred orientations were parameterized only by a single parameter.

We considered using covariance instead of correlation to measure the covariability of neuronal pairs. However, a key advantage of correlation is that it is insensitive to the variance of the spike counts. By contrast, measures that do not normalize for spike-count variance will give larger weights to more variable pairs in any population analysis. In addition, using spike-count correlation allowed us to combine z-scored counts across stimulus conditions. This substantially increased the signal-to-noise ratio of our measurements. As a confirmation that this approach yielded results that generalize, we measured the average, task-aligned spike-count covariance matrix, using the same approach as we used to generate the $r_c$ matrix in Fig. 2c. To estimate the spike-count covariance between a given pair of neurons without including an effect of common stimulus drive, we used an average of the covariance values obtained separately for each stimulus condition, weighted by number of trials. We found that the pattern in the spike-count covariance matrix was closely similar to the $r_c$ matrix (Supplementary Fig. 11). This confirms that our main results are not dependent on the use of $r_c$ measured with normalized spike counts.

Regression model. We used a multilinear regression model to identify fixed and task-dependent components of the structured correlations we observed. We describe the set of observations (811 individual pairwise $r_c$ measurements) in terms of a set of underlying correlation structures: one defining $r_c$ as a function of pairwise preferred orientation alone ('fixed') and the other defining $r_c$ as a function of pairwise preferred orientation relative to the task orientation ('task-dependent'). To provide a continuous and smooth description of the data, each component was parameterized as the sum of an array of $n \times n$ evenly spaced basis functions. Each observation, $y_i$, was expressed as:

$$y_i = x_i^{\text{fixed}} + x_i^{\text{task}} + \epsilon$$  

where $\theta$ and $\phi$ are the preferred orientations of the $i$th pair (relative to the task orientation in the case of the task-dependent loadings), $\mu$ is a pair of orientations defining the location of the $i$th basis function, $z$ is a normalization constant such that the sum of all loadings for observation $i$ ($x_i^{\text{fixed}} + x_i^{\text{task}}$) is 1, and $x$ is the basis function width. Two terms are needed to express the loadings because the data are correlations: the first term describes the upper triangular portion and the second describes the lower triangular portion. Again, angular quantities were doubled, $\mu$ acts as a smoothing hyperparameter. We found that arrays of 8 x 8 were sufficient to describe the structure of the two components. It was sufficient to fit only the upper triangular portion of the array of basis functions. Thus, each component was described by 36 parameters (although the effective number of parameters is substantially lower because of the basis function smoothness and the ridge penalty). We fit the model using ridge regression. The unique optimal solution could therefore be derived analytically as $X = (X'X + \alpha I)^{-1}X'Y$, where $X$ is the concatenated design matrix combining $x_i^{\text{fixed}} + x_i^{\text{task}}$ and $x$ is the ridge parameter, which penalizes the squared amplitude of the basis functions. The optimal values of the hyperparameters of $\alpha$ and $x$ were chosen under 50-fold cross-validation. To ensure that our results were not due to the particular way the above model was constructed, we compared them to those obtained using a conceptually similar regression model. In this alternative model, instead of a grid of basis functions with fixed locations, we described each component as the sum of a variable number of von Mises basis functions, with no correlation and equal width in both dimensions. Thus the $i$th loading ($x_i^{\text{fixed}}(k)$ or $x_i^{\text{task}}(k)$) was given by:

$$x_i(k) = \frac{\epsilon \sin(\theta_i - \phi + \beta)(\cos(x_i - \mu) + \epsilon \cos(\theta_i - \phi + \beta))}{z}$$  

Estimating explainable variance. While the above models did not explain more than a small percentage of the variance of the raw observed $r_c$ values, this is not surprising as the raw correlation data do not vary smoothly with preferred orientation (reflecting both noise and the fact that $r_c$ is known to depend on parameters other than orientation). For this reason, we measured goodness-of-fit relative to an estimate of the explainable variance, which we took as the variance explained simply by a smoothed version of the raw data (sum of values in fixed and task-aligned matrices was 3.6%). Smoothing was performed with a von Mises kernel, with width chosen to maximize variance explained.

Eye movements. Both animals tended to make anticipatory microsaccades near the end of each trial that predicted the upcoming choice, consistent with a prior study. This raised the possibility that choice-related eye movements gave rise to task-dependent changes in retinal input that explained the correlated fluctuations we observed. To rule this out, we measured the task-aligned $r_c$ matrix using a subset of trials on each session for which fixational eye position was not predictive of choice. To identify these trials, we used a linear discriminant analysis (LDA) to predict the subject’s choices using the timeseries of mean binocular eye-position recorded on each trial. Then, we iteratively removed trials, starting with those furthest from the classification boundary, until classification performance no longer exceeded chance. This analysis (Supplementary Fig. 7) was restricted to the first 1.5s of the trial, because we found that considering later timepoints (where most anticipatory microsaccades occurred) required discarding too many trials.

Choice probability predictions. Choice probability was calculated in the standard way. We only used 0% signal trials, as the uneven choice distributions elicited by signal trials yield noisier CP measurements. Assuming feedforward pooling with linear readout weights, the relationship between the covariance matrix for a population of neurons, the readout weight of each neuron and the choice probability (CP) of each neuron is:

$$CP_i = \frac{\sum_{j=1}^{n} \text{sign}(\xi_j) \arctan(2\xi_j^2 - 1)}{\sqrt{\mathbf{C}/\mathbf{C}'\mathbf{C}}}$$  

where $CP_i$ is the CP of neuron $k$ with respect to choice $i$, $\beta$ is the vector of readout weights and $\mathbf{C}$ is the covariance matrix. We used this known relationship to...
quantify the CPs that would be associated with the \( r \) \_structure we observed and the fixed and task-dependent components we identified, assuming only a feedforward source of CP (Fig. 8). CPs, \( r \) \_structure and readout weights were described as task-aligned functions of preferred orientation. This is equivalent to assuming a population of infinite size that is homogeneous at a given orientation. For the fixed component of \( r \), which was indexed relative to raw orientation preferences, we generated a task-aligned version by substituting the observed \( r \) \_values with model fits (using only a fixed component of the model) and then generating a smoothed task-aligned matrix, as in Fig. 2c, using these substituted values. To guarantee real-valued CPs on [0,1], we performed the calculations using a symmetric positive definite approximation\(^5\) of the \( r \) \_matrices, which introduced negligible error.

Since the readout weights were unknown, we generated a random distribution of 1,000 plausible readout weight profiles that could support task performance. To generate a sample from this distribution, we started with a vector of random weights (drawn from a normal distribution) and applied the 90° symmetry inherent in the task, such that \( \theta = -\theta_{\text{ass}} \), where \( \theta \) is the weight assigned to neurons with task-aligned preferred orientation \( \theta \). Then, we smoothed with a wrapped Gaussian kernel with 15° s.d. and excluded profiles that did not have a circular mean within 22.5° of choice 1 (0°). In practice, we found the CP predictions to be insensitive to the readout weights (Supplementary Fig. 9), which is not surprising for a nearly rank-1 matrix (since for exactly rank-1 matrices, the CPs are independent of the weights)\(^1\).

We can use correlations interchangeably with covariances in equation (8), under the simplifying assumption that the variance is uniform as a function of preferred orientation. If \( \Sigma \) is the correlation matrix for a population with uniform variance \( \sigma \), then it follows that:

\[
\xi_k = \frac{\sigma (\Sigma \beta)_k}{\sqrt{(\sigma \Sigma \beta)_k^T (\sigma \Sigma \beta)_k}} = \frac{(\Sigma \beta)_k}{\sqrt{\Sigma_{kk}^T \Sigma_{kk}}}
\]

(9)

where \( \Sigma_{kk} \equiv 1 \) for all \( k \). We felt that spike-count variance that depended systematically on preferred orientation was unlikely to be a feature of the V1 representation and thus that the advantages of using correlations outweighed the cost.

Noise in the decision process after pooling (pooling noise) has the effect of uniformly scaling down CPs, such that \( \xi_k \) in equation (8) is substituted with \( \xi_k \sigma_{\text{pool}} \), where \( \sigma_{\text{pool}} \) is the variance of the pooling noise\(^6\). We found that nonzero pooling noise was needed to avoid overestimating the magnitude of CP from the observed correlation structure. We used a fixed value of pooling noise in our predictions, such that the average squared difference between the CP profile predicted from the observed correlation matrix and the observed CP profile was minimized. Empirically, we found that a pooling noise variance of 0.6 was optimal. Since our spike counts were normalized to have unit variance, this implies a pooling noise whose variance is 60% of the average spike-count variance of single neurons. This should be interpreted with care, as overestimation of CPs may also be an artifact related to the assumption of a homogeneous population\(^1\). Alternatively, the need to invoke pooling noise may be due to nonuniform sensory integration across the trial, which is distinct but which would also have an attenuating effect on CP when measured over the entire trial.

Statistics. Statistical tests were performed nonparametrically using bootstrapping or other resampling methods, as described, with 1,000 resamples. Nonparametric statistical testing is superior when the underlying distribution of the data cannot be assumed. When \( P \) values \(<0.001\) are reported, this indicates the null hypothesis can be ruled out with the most confidence possible given the number of resamples performed. In most cases, resampling was performed from the set of recorded neuronal pairs (\( n = 811 \)), and always with replacement. In all figures, one asterisk indicates significance at the \( P<0.05 \) level, two indicates \( P<0.01 \) and three indicates \( P<0.001 \). When standard error bars are shown, this makes the assumption of normality in the bootstrap distribution of the test statistic. However, this assumption was not formally tested. No statistical methods were used to predetermine sample sizes, but our sample sizes are similar to those of previous publications\(^22,23,27\).

Life Sciences Reporting Summary. Further information on experimental design is available in the Life Sciences Reporting Summary.

Code availability. All computer code used to generate the results is available upon request from the authors.

Data availability. All relevant data are available upon reasonable request from the authors.

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### Experimental design

| Field | Description |
|-------|-------------|
| 1. Sample size | Sample size was 811 pairs of single neurons from two rhesus monkey subjects. Two rhesus monkeys is typical for comparable studies and the number of neuronal pairs far exceeds similar prior studies in awake monkeys. No statistical analysis was performed to predetermine sample size. |
| 2. Data exclusions | To reduce the possibility that a single neuron from the Utah array contributed to two datasets, we included only sessions that were separated by at least 48 hours (with a median separation of 5 days). We excluded from analysis those neurons whose mean evoked firing rate did not exceed 7 spikes/second or which were poorly orientation tuned (preferred orientation could not be estimated to within a standard error of 5 degrees). We finally excluded some sessions where behavioral was poor. These exclusion criteria are described in greater detail in Online Methods. |
| 3. Replication | The main results were reliably reproduced in both subjects, as described in the manuscript and the Supplementary Materials. |
| 4. Randomization | Because our study was on the task-dependence of neuronal activity, each subject was its own control. The control consisted of identical measurements made across task contexts and in the absence of any task, as described in detail in the Methods. |
| 5. Blinding | Investigators were not blind. |

Note: all in vivo studies must report how sample size was determined and whether blinding and randomization were used.
6. Statistical parameters

For all figures and tables that use statistical methods, confirm that the following items are present in relevant figure legends (or in the Methods section if additional space is needed).

| n/a | Confirmed |
|-----|-----------|
| ☐   | ☒         |
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- The exact sample size (n) for each experimental group/condition, given as a discrete number and unit of measurement (animals, litters, cultures, etc.)
- A description of how samples were collected, noting whether measurements were taken from distinct samples or whether the same sample was measured repeatedly
- A statement indicating how many times each experiment was replicated
- The statistical test(s) used and whether they are one- or two-sided
- Only common tests should be described solely by name; describe more complex techniques in the Methods section.
- A description of any assumptions or corrections, such as an adjustment for multiple comparisons
- Test values indicating whether an effect is present
- Provide confidence intervals or give results of significance tests (e.g. P values) as exact values whenever appropriate and with effect sizes noted.
- A clear description of statistics including central tendency (e.g. median, mean) and variation (e.g. standard deviation, interquartile range)
- Clearly defined error bars in all relevant figure captions (with explicit mention of central tendency and variation)

See the web collection on statistics for biologists for further resources and guidance.

7. Software

Policy information about availability of computer code

Describe the software used to analyze the data in this study.

Stimulus generation and behavioral control were performed using custom software written in Matlab and C. Neural data acquisition was done using Spike2 (Cambridge Electronics Design) and Cerebus (Blackrock). All spike sorting and data analysis was performed using custom software written in Matlab. Code is compatible with Matlab version 2014b and above.

For manuscripts utilizing custom algorithms or software that are central to the paper but not yet described in the published literature, software must be made available to editors and reviewers upon request. We strongly encourage code deposition in a community repository (e.g. GitHub). Nature Methods guidance for providing algorithms and software for publication provides further information on this topic.

8. Materials availability

Indicate whether there are restrictions on availability of unique materials or if these materials are only available for distribution by a third party.

No unique materials were used.

9. Antibodies

Describe the antibodies used and how they were validated for use in the system under study (i.e. assay and species).

No antibodies were used.

10. Eukaryotic cell lines

a. State the source of each eukaryotic cell line used.

No cell lines were used.

b. Describe the method of cell line authentication used.

Describe the authentication procedures for each cell line used OR declare that none of the cell lines used have been authenticated OR state that no eukaryotic cell lines were used.

c. Report whether the cell lines were tested for mycoplasma contamination.

Confirm that all cell lines tested negative for mycoplasma contamination OR describe the results of the testing for mycoplasma contamination OR declare that the cell lines were not tested for mycoplasma contamination OR state that no eukaryotic cell lines were used.

d. If any of the cell lines used are listed in the database of commonly misidentified cell lines maintained by ICLAC, provide a scientific rationale for their use.

Provide a rationale for the use of commonly misidentified cell lines OR state that no commonly misidentified cell lines were used.
Animals and human research participants

Policy information about studies involving animals; when reporting animal research, follow the ARRIVE guidelines

11. Description of research animals

Provide all relevant details on animals and/or animal-derived materials used in the study.

Two male macaque monkeys (Macaca mulatta) were used. One ('jbe') was pair housed, while the other ('lem') could not be, due to antisocial behavior. Both animals were housed in the 12 hour light cycle and given at least weekly access to a play area. Monkey 'jbe' was 16 while monkey 'lem' was 14 for the majority of recording sessions. All procedures (described in greater detail in Methods) were performed in accordance with the U.S. Public Health Service Policy on the humane care and use of laboratory animals and all protocols were approved by the National Eye Institute Animal Care and Use Committee.

Policy information about studies involving human research participants

12. Description of human research participants

Describe the covariate-relevant population characteristics of the human research participants.

No human subjects were used.