Enhanced electromechanical response of ferroelectrics due to charged domain walls

Tomas Sluka¹, Alexander K. Tagantsev¹, Dragan Damjanovic¹, Maxim Gureev¹ & Nava Setter¹

While commonly used piezoelectric materials contain lead, non-hazardous, high-performance piezoelectrics are yet to be discovered. Charged domain walls in ferroelectrics are considered inactive with regards to the piezoelectric response and, therefore, are largely ignored in this search. Here we demonstrate a mechanism that leads to a strong enhancement of the dielectric and piezoelectric properties in ferroelectrics with increasing density of charged domain walls. We show that an incomplete compensation of bound polarization charge at these walls creates a stable built-in depolarizing field across each domain leading to increased electromechanical response. Our model clarifies a long-standing unexplained effect of domain wall density on macroscopic properties of domain-engineered ferroelectrics. We show that non-toxic ferroelectrics like BaTiO₃ with dense patterns of charged domain walls are expected to have strongly enhanced piezoelectric properties, thus suggesting a new route to high-performance, lead-free ferroelectrics.

¹ Ceramics Laboratory, Swiss Federal Institute of Technology, Lausanne, CH-1015 Switzerland. Correspondence and requests for materials should be addressed to T.S. (email: tomas.sluka@epfl.ch).
In the last two decades, sensors and actuators based on lead-containing ferroelectrics gained a dominant position in applications ranging from delicate positioning systems, ultrasonic medical diagnostic tools and microsurgery devices to robust fuel injectors. These lead-containing materials have to be replaced by environmentally benign alternatives\(^1\)\(^-\)\(^\text{2}\). So far, the search for lead-free ferroelectrics was mainly focused on the synthesis of new compositions exhibiting high-intrinsic piezoelectric properties\(^3\)\(^-\)\(^\text{5}\). The possibility to enhance piezoelectric properties of known lead-free ferroelectric crystals by so-called frustrated poling and domain engineering has also been explored\(^6\)\(^-\)\(^\text{10}\). In this approach, the poling electric field is applied along a nonpolar direction, which forms equal angles with at least two possible orientations of spontaneous polarization. During this poling, two or more ferroelectric states are equally preferred, creating an artificial domain structure with several coexisting domain states. Such a structure is macroscopically polar (has non-zero net polarization) and includes a certain volume fraction of domain walls.

It has been found that, in the classical lead-free perovskite ferroelectric BaTiO\(_3\), a high density of domain walls with spacing in the micrometre range can result in up to a fourfold enhancement of functional properties\(^9\), while it was established that the enhancement is not associated with the domain wall motion. However, the body of available experimental data is insufficient to clearly relate the observed effects to features of the domain patterns in the samples. This experimental activity has drawn much attention by theorists\(^1\)\(^-\)\(^\text{15}\) who were unable to explain the experimental observations unless unrealistic assumptions were taken. Thus, despite intriguing experimental findings, the future of fine-scale domain patterns as systems with enhanced electromechanical properties remains obscure.

Here we demonstrate the existence of an enhancement mechanism of the dielectric and piezoelectric response in ferroelectrics with fine-scale charged domain-wall patterns. This mechanism provides a realistic interpretation of the experimental observations and outlines a new direction in the search for high electromechanical response in lead-free ferroelectrics.

In the experimental reports on enhanced properties due to engineered domain structures, we recognized that head-to-head and tail-to-tail domain configurations\(^1\)\(^6\)\(^-\)\(^\text{19}\) such as those shown in Fig. 1, must have been formed during the frustrated poling process of BaTiO\(_3\) (refs 8,10). The reports\(^8\)\(^,\)\(^\text{10}\) describe poling techniques leading to the controlled formation of domain structures with various domain-wall densities. Analysis of the domain walls and crystal orientations leads to indirect identification of 90°-charged domain walls\(^1\)\(^0\) which occupy an unspecified fraction of crystal volume. However, the significance of this formation of charged domain walls passed entirely un-noticed.

Here we report an analysis, based on Landau–Ginzburg–Devonshire theory and the theory of semiconductors, which establishes that the dielectric and piezoelectric response of such systems with charged domain walls increase strongly on the reduction of the domain period. This is expected to happen under two conditions: the ferroelectric phase transition in the material should be of first order and a strong dielectric anisotropy must exist, namely the dielectric constant in the direction perpendicular to the spontaneous polarization, \(\varepsilon_{\text{r}}\), should be much larger than that in the direction parallel to it, \(\varepsilon_{\text{c}}\). Both these conditions are met for BaTiO\(_3\) (ref. 20) and KNbO\(_3\) (ref. 21).

### Results

#### Charged domain walls

Charged domain walls contain a high density of bound charges, which must be strongly compensated by free carriers to prevent a huge depolarizing field that would prohibit formation of dense periodic domain structures. For realistic parameters of ferroelectric perovskites (unless these are heavily doped), such compensation cannot be provided with the typical carrier concentration in these materials\(^1\)\(^6\)\(^,\)\(^\text{22}\). Most of the screening charge originates from electron transfer across the forbidden energy gap, \(E_g\). This means that, at the head-to-head wall (positive bound charge), the bottom of the conduction band of the material should approach the Fermi level, providing electrons for the screening. Analogously, at the tail-to-tail wall (negative bound charge), the top of the valence band approaches the Fermi level, providing screening holes. This implies the existence of a potential difference of about \(E_g/g\) (\(g\) is the elementary charge) between such couple of walls. As a result, the domain between these walls is exposed to an electric field, \(E_{\text{dep}}\), which depends on the forbidden gap and the domain width, \(w\), as expressed in equation (1),

\[
E_{\text{dep}} \approx E_g/gw. \tag{1}
\]

This field is a result of the incomplete compensation of bound polarization charge with free carriers at the domain walls. The imperfect compensation is a principal feature of the system because a perfect compensation would result in zero-band bending, and then the free carriers needed for compensation would not be available.
at all. Therefore, the system keeps an optimal trade-off between imperfect screening and a minimal necessary band bending. In the case of an electrode at \(110_\alpha\) (the subscript \(\alpha\) denotes the pseudocubic orientation) plate of tetragonal BaTiO\(_3\) (Fig. 1a) containing a pattern of charged domain walls (Fig. 1b), \(E_p = 3\) eV and with domain width \(w\) of several micrometres, the depolarizing field \(E_{\text{dep}}\) can readily reach values of 10–20 kV cm\(^{-1}\) (equation (1)). It is this built-in field (growing with domain-wall density) that induces a polarization rotation leading to enhanced dielectric and piezoelectric response of each domain.

**Polarization rotation.** The mechanism of polarization rotation is qualitatively illustrated in Fig. 2 for the case of tetragonal BaTiO\(_3\). The contour plot of bulk free-energy density, Fig. 2a, shows two global minima corresponding to two different orientations of polarization in the tetragonal phase and one local minimum for the orthorhombic phase. The minimal energy path for polarization switching between the two tetragonal states inevitably follows a rotation-like path across the orthorhombic minimum. The key factor responsible for the enhanced properties is that polarization rotated by \(E_{\text{dep}}\) approaches a point of instability between tetragonal and orthorhombic phases. At this point, a small excitation by an external electric field in the [110] direction is able to induce a large change of polarization along the dash-dotted line in Fig. 2. The essential characteristic of a material that allows the enhancement effect is illustrated in Fig. 2b. It shows a surface that encloses a region where values of polarization lead to energy lower than \(-2.18\text{ MJ m}^{-3}\). Polarization is stable in the tetragonal minima (white circles), but follows a minimal energy path during switching between the tetragonal states. The important feature is the non-zero change of the \(P_3\)-component during switching. The energy profile corresponds to BaTiO\(_3\), but a qualitatively equivalent situation is available, for example, in a (111) plate of KNbO\(_3\).

In view of the strong dielectric anisotropy of BaTiO\(_3\) (experimentally at room temperature \(\varepsilon_{33}/\varepsilon_{\alpha} = 30\)) (ref. 20), it is the value of \(\varepsilon_{\alpha}\) that controls the total dielectric response of the system. For this reason, we discuss the impact of the built-in field \(E_{\text{dep}}\) on this quantity alone. Let us consider the case where the application of the field leads to small changes of the ferroelectric polarization. In this approximation, the relative reduction of the absolute value of polarization can be evaluated as \(\delta = E_{\text{dep}}\varepsilon_{\alpha}/(\sqrt{2}P_0)\) (\(P_0\) is the spontaneous polarization) with the transverse component being \(\gamma\varepsilon P_0\) where \(\gamma = \varepsilon_{\alpha}/\varepsilon_{\alpha}\) is the dielectric anisotropy factor. Using the polarization equation of state in the X–Z plane, one can readily describe an impact of the built-in field on \(\varepsilon_{\alpha}\) in terms of the following relation between the modified value of the transverse component of the dielectric constant \(\varepsilon_{\alpha}\) and \(\delta\):

\[
\varepsilon_{\alpha}(\delta) = \frac{\varepsilon_{\alpha}(0)}{1 - A\gamma\delta - B\gamma(\gamma\delta)^2}. \tag{2}
\]

Here factors \(A\) and \(B\) can be readily expressed in terms of the coefficient of the Landau expansion \(^3^3\) for BaTiO\(_3\) at room temperature \(A = 0.3\) and \(B = 0.6\). The sign of the coefficient \(B\) has an essential role in the enhancement mechanism and it can only be positive in materials that exhibit a first-order phase transition. The \(A\)-containing term in equation (2) describes the elongation and contraction of polarization, whereas the \(B\)-containing term controls the effect of polarization rotation. In the linear approximation, the rotation angle \(\theta\) can be expressed in terms of relative change of the polarization \(\delta\): \(\theta = \gamma\delta\). Keeping this in mind, one sees that the positive sign of \(B\) implies that the polarization rotation leads to a permittivity enhancement. Conversely, if the ferroelectric transition in the material were of the second order, \(B\) would be negative and the polarization rotation would not lead to enhancement of permittivity.

With a large value of \(\gamma\) one concludes from the equation (2) that polarization rotation is the leading effect. The angle corresponding to substantial enhancement of \(\varepsilon_{\alpha}\) can be evaluated from the condition \(B\gamma\delta^2 = 1\), yielding \(\theta = 13^\circ\) for BaTiO\(_3\). Such a level of polarization rotation can be reached under realistic values of the built-in field. This is clear from Fig. 3a, which shows the calculated dependence of \(\theta\) on \(E_{\text{dep}}\). Thus for the domain pattern addressed, the electric field arising from incomplete compensation of the bound charge on head-to-head and tail-to-tail walls is strong enough to dramatically enhance the dielectric response of the system. Similar effects of enhancement of the dielectric and piezoelectric properties can be expected also in KNbO\(_3\) and in ferroelectrics at their morphotropic boundary.

The semi-quantitative arguments following from equation (2) are supported by more detailed Landau-theory calculations (see Methods) that show the unlimited growth of the transverse component of the dielectric constant when approaching a critical angle as shown in Fig. 3b.

**Properties of ferroelectrics with charged domain walls.** We verified the enhancement mechanism described above by means of phase-field simulations of a poly-domain system, where the ferroelectric was treated as a wide-bandgap semiconductor in the effective mass approximation (see Methods). First, stability of 90°-charged domain walls was confirmed. Then, we have calculated piezoelectric, \(d_{31}\) and \(d_{33}\), and dielectric \(\varepsilon_{33}\) coefficients as functions of domain-wall spacing \(w\), which are experimentally measurable parameters of...
the system. The phase field results (circles and squares in Fig. 4a–c) include contributions of domain response and intrinsic response of domain walls. To identify the magnitudes of these contributions, we performed the Landau-theory calculations for a single domain that is artificially exposed to depolarizing electric field applied along x axis (Fig. 1b). The magnitude of this electric field was obtained from phase-field simulation as approximately $E_{\text{dep}}=\Delta V_{\text{eff}}/w$ where $\Delta V_{\text{eff}}=3.5$ V is an effective potential difference between domain walls. This potential difference is larger than $E_{\text{g}}/q=3$ V due to the shape of the band bending (Fig. 1c). However, as seen in Fig. 4a–c, the intrinsic domain wall contribution, which is the difference between single-domain and poly-domain response, is negligible. This conclusion is surprising with respect to the huge domain-wall thickness (Fig. 4d), but it agrees with studies done in the past\textsuperscript{11–13}, where intrinsic domain-wall response failed to explain the experimental observations\textsuperscript{7–10}. The large thickness of charged domain walls, $DW>100$ nm, compared with neutral ones, $DW=1$ nm, is qualitatively consistent with a recently published theory\textsuperscript{16} that explains the widening mechanism of charged domain walls in detail. Our calculations also show temperature $T$ and $E_{\text{g}}$ dependence of the smallest theoretically possible domain-size $w_{\text{lim}}$ (Fig. 4e).

The phase-field calculated band-bending profile and free-charge concentrations are shown in Fig. 1c, where the difference between the edge of the conduction (or valence) band and the Fermi level in the wall centre, $\Delta E$, can be evaluated for the condition that the charge density of the free carriers at this point, $q(2m_{\text{eff}}\Delta E)^{3/2}/(3\pi^{2}h^{3})^{1}$ ($m_{\text{eff}}$ and $h$ are the effective mass of electrones/holes, and the reduced Planck constant, respectively) is about the mean bound charge density in the walls, $\langle 2P_{j}/w \rangle$. Such estimates, with $m_{\text{eff}}=0.12 m_{e}$ ($m_{e}$ is the free electron mass), $w=100$ nm and $P_{j}=0.26$ C m$^{-2}$, yield $\Delta E=0.24$ eV in reasonable agreement with the results of phase-field simulation where $\Delta E=0.22$ eV.

**Figure 3** | Depolarizing field-induced polarization rotation and impact on permittivity. The angle $\theta$ growing with $E_{\text{dep}}$ (a) which results in an increase of the transverse dielectric response $\varepsilon_{33}$ (b). Displayed curves correspond to temperatures 278 K (blue), 288 K (green), 298 K (red), and 308 K (orange).

**Figure 4** | Enhancement of macroscopic properties with decreasing domain size. Relative permittivity $\varepsilon_{33}$ (a), and piezoelectric coefficients $d_{33}$ (b), and $d_{31}$ (c), are plotted as a function of domain width $w$. The solid lines represent the inner response of a domain that is exposed to built-in depolarizing field owing to imperfectly compensated charged domain walls. Displayed curves correspond to temperatures 278 K (blue lines), 288 K (green lines), 298 K (red lines), and 308 K (orange lines). Red circles and green squares represent phase-field simulation results that include intrinsic contributions of charged domain walls at temperatures 288 K (green squares) and 298 K (red circles). Domain-wall width $DW$ against domain width $w$ (d), shows small domain-wall broadening when critical domain width is approached. (e) The critical (minimal) domain width $w_{\text{lim}}$ against temperature $T$ is shown for bandgaps 2 eV (dash-dotted), 3 eV (dashed), and 4 eV (solid).
The large concentration of free carriers at charged domain walls (Fig. 1c) may raise the question as to whether the expected high domain-wall conductivity cannot short-circuit the electrodes and hence make the enhancement phenomena practically unavailable. To answer this question, we simulated a finite-6 µm thick–electroded sample. One can see, in a colour-scale map in Fig. 5, that the free-carrier concentration dramatically drops in the vicinity of the electrodes. These gaps are formed because of the flat profile of the electric potential (constant potential) at the electrodes that prohibits band-bending and, hence, a high concentration of free-carriers in the vicinity of the electrodes. The results in Fig. 5 correspond to the situation where the work functions of the electrode and ferroelectric are identical, but, in general, the size of the gaps is dependent on the difference between the work functions.

Discussion

Our analysis shows that the built-in electric field, created in periodic domain patterns with charged domain walls, grows significantly with increasing domain-wall density. Once the domain period is in the range of several micrometres, the built-in field can lead to an appreciable enhancement of the dielectric and piezoelectric response of the polydomain system. We identify the features that control this phenomenon, namely a very high dielectric anisotropy factor \( \gamma = E_c/E_E \) and a first-order ferroelectric phase transition.

The presented results are qualitatively in good agreement with experimental observations of domain-wall density effects on macroscopic properties of [111]-poled BaTiO\(_3\) crystals (Fig. 6). In these experiments, the piezoelectric and dielectric constants were subject to a fourfold enhancement when domain size reached three-to-five microns. We suggest the presented mechanism as a new degree of freedom in the search for ferroelectrics with high piezoelectric response that is particularly attractive in light of the need for lead-free piezoelectrics.

Methods

The phase-field model. The presented results were obtained primarily by means of phase-field simulation that incorporates coupling between ferroelectric and wide-bandgap semiconductor properties. Our simulation includes elastic interactions that results in stable 90°-charged domain walls.

Model equations are obtained by Lagrange principle from Helmholtz free-energy density:

\[
\mathcal{F} = \mathcal{F}_{\text{bulk}} + \mathcal{F}_{\text{ele}} + \mathcal{F}_{\text{es}} + \mathcal{F}_{\text{grad}} + \mathcal{F}_{\text{ele}}.
\]

where \( P_{i,j} \) is the polarization, \( P_{i,j} \) its derivatives (the subscript \( ' \) represents the operator of spatial derivatives \( \partial / \partial x_j \)), \( D \) the electric displacement and \( \varepsilon_0 = 1 / 2(\varepsilon_{ij} + \varepsilon_{ji}) \) is the elastic strain where \( \varepsilon_i \) is a displacement vector.

The bulk free-energy density

\[
f_{\text{bulk}}(\varepsilon_{ij}) = \alpha_0 \sum_{i,j} \varepsilon_{ij}^2 + \alpha_{11} \sum_{i,j} \varepsilon_{ij}^4 + \alpha_{12} \sum_{i,j} \varepsilon_{ij}^2 \varepsilon_{ij}^2 + \alpha_{111} \sum_{i} \varepsilon_{i}^6
\]

\[
+ \alpha_{112} \sum_{i,j} \varepsilon_{ij}^2 \varepsilon_{ij}^2 + \alpha_{23} \sum_{i,j} \varepsilon_{ij}^2 + \alpha_{23} \sum_{i} \varepsilon_{i}^4
\]

is expressed for a zero strain as a six-order polynomial expansion, where \( \alpha_0, \alpha_{11}, \alpha_{12}, \alpha_{111}, \alpha_{123}, \alpha_{23} \) are parameters fitted to the single-crystal properties (Table 1). The remaining contributions represent bilinear forms of elastic energy \( f_{\text{ele}}(\varepsilon_{ij}) = \varepsilon_{ij} \rho_{ij} P_{i,j} \), where \( \rho_{ij} \) is the elastic stiffness, electrostriction energy \( f_{\text{grad}}(\varepsilon_{ij}) = \varepsilon_{ij} \rho_{ij} P_{i,j} \), where \( \rho_{ij} \) is the electrostriction coefficients, gradient energy \( f_{\text{grad}}(\varepsilon_{ij}) = \varepsilon_{ij} \rho_{ij} P_{i,j} \), where \( \rho_{ij} \) are the gradient energy coefficients, and electrostatic energy \( f_{\text{ele}}(\varepsilon_{ij}) = 1 / 2(\varepsilon_{ij} \rho_{ij} P_{i,j} - D_j P^2) \), where \( \varepsilon_{ij} \) and \( \rho_{ij} \) are permittivity of vacuum and relative background permittivity, respectively. The zero-strain coefficients \( \alpha_0^0 \) can be expressed in terms of usually introduced stress-free coefficients \( \alpha_0 \) as follows:

\[
\alpha_0^0 = \alpha_0 + 1 / 6 \left( \frac{2(\xi_{11} - \xi_{12})^2}{\xi_{11}^2 - \xi_{12}^2} + \frac{(\xi_{11} + 2\xi_{12})^2}{\xi_{11}^2 + 2\xi_{12}^2} \right)
\]

\[
\alpha_0^0 = \alpha_0 + 1 / 6 \left( \frac{2(\xi_{11} + 2\xi_{12})^2}{\xi_{11}^2 + 2\xi_{12}^2} - \frac{2(\xi_{11} - \xi_{12})^2}{\xi_{11}^2 + \xi_{12}^2} \right)
\]

\[\alpha_0^0 = \alpha_0 + 1 / 6 \left( \frac{3\xi_{11}^2}{4\xi_{11}^2} \right)
\]

By using the Legendre transformation to electric enthalpy

\[h[(P_i, P_{ij}, \varepsilon_{ij}, \phi)] = f[(P_i, P_{ij}, \varepsilon_{ij}, \phi)] - D_j E_j,
\]

where \( E_j = -\varphi_j \) is the electric field and \( \varphi \) the electric potential, and using Lagrange principle, we can uniformly express the set of field equations that govern...
the kinetics of ferroelectrics:

\[
\left( \frac{\partial h}{\partial \omega} \right)_{ij} = 0,
\]

\[
\left( \frac{\partial h}{\partial E_{ii}} \right) = q(p - n),
\]

\[
\frac{1}{\Gamma} \frac{\partial P_i}{\partial t} = \left( \frac{\partial h}{\partial P_{ij}} \right)_{ij} = -\frac{\partial h}{\partial P_i}.
\]  

Equation (5) defines the mechanical equilibrium while inertia is neglected. Equation (6) expresses Gauss's law of a dielectric including a non-zero concentration of free electrons n and holes p. Equation (7) is the time-dependent Landau–Ginzburg–Devonshire equation\(^{25}\) which governs the spatiotemporal evolution of spontaneous polarization with kinetics given by coefficient \(\Gamma\).

Coupling between the ferroelectric/ferroelastic system with its semiconductor properties is introduced by considering a non-zero density of free carriers (electron-hole) in the electrostatic equation (6). The semiconductor properties were introduced under the assumption of zero concentration of dopants, which was shown to be an acceptable approximation to a small concentration of defects and dopants\(^{17}\). The distribution of free carriers is governed by continuity equations:

\[
\frac{q}{\tau} \frac{\partial n}{\partial t} + j^{(e)}_{ij} = q R_n,
\]

\[
\frac{q}{\tau} \frac{\partial p}{\partial t} + j^{(h)}_{ij} = q R_p,
\]

where electron and hole currents \(j^{(e)}_{ij}\) and \(j^{(h)}_{ij}\), respectively, are governed by drift and diffusion as follows:

\[
j^{(e)}_{ij} = \mu_e (q E_{ii} + k_0 T n_j) \quad \text{and} \quad j^{(h)}_{ij} = \mu_h (q E_{ii} - k_0 T p_j).
\]

Here \(\mu_e\) and \(\mu_h\) are electron and hole mobilities, respectively. Because we analyse only the stationary solution in thermal equilibrium, we can introduce computationally convenient form of recombination rates \(R_n\) and \(R_p\) as follows:

\[
R_n = -(n - n_0) / \tau \quad \text{and} \quad R_p = -(p - p_0) / \tau,
\]

where \(\tau\) is life-time constant and \(n_0\) and \(p_0\) are electron and hole concentrations in thermal equilibrium:

\[
n_0 = N F_{1/2} \left( -E_n - E_k - q \varphi \right) / k_0 T,
\]

\[
p_0 = N F_{1/2} \left( -E_V - E_f + q \varphi \right) / k_0 T.
\]

Here \(F_{1/2}\) is the Fermi–Dirac integral. Density of states is given by effective mass approximation:

\[
N \approx 2 \left( \frac{m_{\text{eff}} q k_0 T}{2 \pi h^2} \right)^{3/2},
\]

where effective mass \(m_{\text{eff}} = m_0\) is assumed equal for electrons and holes. As the effective mass of free carriers in BaTiO\(_3\) varies in literature, we tested the model with a wide range of effective mass constants, \(c_V (0.05, 50)\), showing an insignificant impact on the enhancement phenomena. However, the constant \(c\) controls the screening regime (classical/degenerate) and width of the domain walls. Results presented in the graphs correspond to \(c = 0.117\), that is, \(N = 10^{24} \text{m}^{-3}\) used by Xiao et al.\(^{26}\)

The ferroelectric-semiconductor model was designed as a subdomain of size \(2 \times 0.25 \text{\mu m}^2\) with applied periodic boundary conditions joining the solution of all solved variables between opposite parallel boundaries. The numerical solution of equations (5)–(9) on the defined subdomain was performed by a finite element method with linear triangular elements of size \(6 \text{ nm}\) in the vicinity of domain walls and \(40 \text{ nm}\) inside domains. The simulation starts from initial conditions that are defined as zero for all variables except polarization which is \(P = \sqrt{2}(1, 0, 0)\) and \(P = \sqrt{2}(-1, 0, 0)\) for \(P_0 = 0.262 \text{C m}^{-2}\), in regions separated by 70 nm gap, where \(P = 0\). The simulation reaches thermal equilibrium in \(<5\,\text{ns}\) and gives solutions for the spatial distribution of polarization, \(P\), mechanical displacement, \(u\), electric potential, \(\varphi\), and concentrations of electrons \(n\) and holes \(p\). We used these to calculate the band-bending and charge concentrations in Fig. 1c and domain-wall width and critical domain size in Fig. 4d. Then the domain structure is exposed to (i) small compressive stress, 100 kPa, and (ii) small electric field, 4 V mm\(^{-1}\), when the average change of electric displacement is integrated and (i) the direct piezoelectric and (ii) dielectric coefficients are calculated (Fig. 4a–c). This calculation also shows almost zero domain-wall widening when small electric field or stress are applied.

The single-domain Landau-theory approximation. The phase-field results are accompanied by Landau-theory calculations of a single domain, which is subjected to an artificially introduced depolarizing field obtained from the phase-field model. This approach calculates macroscopic properties of domains by minimization of Gibbs free energy. It allows domain wall and domain contributions to be distinguished. The Gibbs free energy of homogeneous stress-free sample is defined as

\[
G(P, E) = f_{\text{bulk}}(P) - D_e (P, E) E_i.
\]

Here the non-indexed symbols \(f, E\) represent vectors. The bulk free-energy density \(f_{\text{bulk}}\) is defined as \(f_{\text{bulk}} = f_{\text{bulk}}^e + f_{\text{bulk}}^f + f_{\text{bulk}}^\varphi\) for stress-free homogeneous sample, that is, at \(e_0 = Q_{\varphi 0}(P_0).\) Here \(Q_{\varphi 0}\) are the coefficients of the direct electrostriction effect.

The calculation searches for the minimum of \(G(P, E)\) for non-zero electric field \(E\) that gives polarization as follows:

\[
P(E) = \arg \min_{P > 0} G(P, E), \text{if min exists}.
\]

Using \(P(E)\) and strain induced by electrostriction effect \(e_0(E) = Q_{\varphi 0}(P(E))E\), we calculate effective piezoelectric coefficients:

\[
\varepsilon_{\text{eff}}(E_{\text{dep}}) = \frac{\varepsilon_0 (E_{\text{dep}} + \Delta E) - \varepsilon_0 (E_{\text{dep}})}{\Delta E},
\]

where the starred symbols are expressed in the coordinate system of a (110) crystal.

The presented results correspond to phenomenological parameters as introduced in Table 1.

References

1. Eu-directive 2002/95/EC: restriction of the use of certain hazardous substances in electrical and electronic equipment (RoHS). Off. J. Eur. Union 46, 19–23 (2003).
2. Eu-directive 2002/96/ce: waste electrical and electronic equipment (WEEE). Off. J. Eur. Union 46, 24–38 (2003).
3. Rodel, J., Jo, W., Seifert, K. T. P., Anton, E. M., Granzow, T. & Damjanovic, D. Perspective on the development of lead-free piezoceramics. J. Am. Ceram. Soc. 92, 1153–1177 (2009).
4. Saito, Y. et al. Lead-free piezoceramics. Nature 432, 84–87 (2004).
5. Liu, W. F. & Ren, X. B. Large piezoelectric effect in Pb-free ceramics. J. Appl. Phys. 86, 2746–2750 (1999).
6. Park, S. E., Wada, S., Cross, L. E. & Shrout, T. R. Crystallographically engineered BaTiO₃ single crystals for high-performance piezoelectrics. J. Appl. Phys. 83, 64102 (2008).
7. Xiang, Y., Zhang, R. & Cao, W. W. Piezoelectric properties of domain engineered PZN-PT single crystals. Ferroelectrics 251, 93–100 (2001).
8. Wada, S. & Tsurumi, T. Enhanced electromechanical response of BaTiO₃ single crystals with engineered domain configuration. Br. Ceram. Trans. 103, 93–96 (2004).
9. Tagantsev, A. K. & Setter, N. Head-to-head and tail-to-tail 180 degrees domain walls in BaTiO₃ thin films. Appl. Phys. Lett. 90, 041915 (2007).
10. Park, S. E., Wada, S., Cross, L. E. & Shrout, T. R. Crystallographically engineered BaTiO₃ single crystals for high-performance piezoelectrics. J. Appl. Phys. 86, 2746–2750 (1999).
11. Abluwaile, R., Lookman, T., Saxena, A. & Cao, W. W. Domain-size dependence of piezoelectric properties of ferroelectrics. Phys. Rev. B 72, 014112 (2005).
12. Abluwaile, R., Lookman, T., Saxena, A. & Cao, W. W. Domain-size dependence of piezoelectric properties of ferroelectrics. Phys. Rev. B 72, 014112 (2005).
13. Hlinka, J., Ondrejkovic, P. & Marton, P. The piezoelectric response of nanotwinned BaTiO₃. Nanotechnology 20, 105709 (2009).
14. Yang, Y., Zhang, R. & Cao, W. W. Piezoelectric properties of domain engineered barium titanate single crystals with different volume fractions of domain walls. J. Appl. Phys. 106, 61102 (2009).
15. Shika, T., Damjanovic, D., Tagantsev, A., Colla, E., Mtebwa, M. & Setter, N. The stress-assisted enhancement of piezoelectric properties due to mechanically incompatible domain structures in BaTiO₃. IEEE International Symposium on the Applications of Ferroelectrics (ISAf) AUG 09-12 (Edinburgh, Scotland 2010).
16. Gureev, M. Y., Tagantsev, A. K. & Setter, N. Head-to-head and tail-to-tail 180 degrees domain walls in an isolated ferroelectric. Phys. Rev. B 83, 184104 (2011).
17. Eliseev, E. A., Morozovska, A. N., Svechnikov, G. S., Gopalan, V. & Shur, V. Y. Static conductivity of charged domain walls in uniaxial ferroelectric semiconductors. Phys. Rev. B 83, 235313 (2011).
18. Yin, J. H. & Cao, W. W. Observation and analysis of domain configurations in domain engineered PZN-PT single crystals. Ferroelectrics 251, 93–100 (2001).
19. Jia, C. L. et al. Atomic-scale study of electric dipoles near charged and uncharged domain walls in ferroelectric films. Nat. Mater. 7, 57–61 (2008).
20. Zgonik, M. et al. Dielectric, elastic, piezoelectric, electrooptic, and elasto-optic tensors of BaTiO₃ crystals. Phys. Rev. B 50, 5941–5949 (1994).
21. Zgonik, M. et al. Materials constants of KNbO₃ relevant for electrooptics and acoustooptics. J. Appl. Phys. 74, 1287–1297 (1993).
22. Vul, B. M., Guro, G. M. & Ivanchik, I. Encountering domains in ferroelectrics. Ferroelectrics 6, 29–31 (1973).
23. Bell, A. J. & Cross, L. E. A phenomenological gibs function for BaTiO₃ giving correct E-field dependence of all ferroelectric phase-changes. Ferroelectrics 59, 197–203 (1984).
24. Li, Y. L. & Chen, L. Q. Temperature-strain phase diagram for BaTiO₃ thin films. Appl. Phys. Lett. 88, 072905 (2006).
25. Semenovskaya, S. & Khachaturyan, A. G. Development of ferroelectric mixed states in a random field of static defects. J. Appl. Phys. 83, 5125–5136 (1998).
26. Xiao, Y., Shenoy, V. B. & Bhattacharya, K. Depletion layers and domain walls in semiconducting ferroelectric thin films. Phys. Rev. Lett. 95, 247603 (2005).

Acknowledgements
This material is based on work supported by the Swiss National Science Foundation project number 200021-125931 and EU project ERC-268058 MOBILE-W.

Author contributions
N.S. initiated and supervised the project and contributed to the manuscript. A.K.T. initiated work on charged domain walls. D.D., A.K.T. and T.S. suggested the principle idea and wrote the manuscript. T.S. designed, performed and analysed simulations. N.S. initiated and supervised the project and contributed to the manuscript. A.K.T. provided project number 200021-125931 and EU project ERC-268058 MOBILE-W.

Additional information
Competing financial interests: The authors declare no competing financial interests.

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How to cite this article: Sluka, T et al. Enhanced electromechanical response of ferroelectrics due to charged domain walls. Nat. Commun. 3:748 doi: 10.1038/ncomms1751 (2012).

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