A Novel Evaporative Cooling System with a Polymer Hollow Fibre Spindle

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Abstract: A novel evaporative cooling system, in which the hollow fibre module constitutes as the humidifier and evaporative cooler, is proposed. With the aim to avoid the flow channelling or shielding of adjacent fibres the fibres inside each bundle were made into a spindle shape to allow maximum contact between the air stream and the fibres. This novel hollow fibre integrated evaporative cooling system will provide a comfortable indoor environment for hot and dry area. Moreover, the water vapour can permeate through the hollow fibre effectively, and the liquid water droplets will be prevented from mixing with the processed air. Under various inlet air dry bulb temperatures (27\degree C, 30\degree C, 33\degree C, 36\degree C and 39\degree C), and various inlet air relative humidity (23\%, 32\% and 40\%), the cooling performances of the proposed novel evaporative cooling system were experimentally investigated. The variations of outlet air dry bulb temperature, wet bulb effectiveness, dew point effectiveness and cooling capacity with respect to different incoming air dry bulb temperature were studied. The effects of various incoming air Reynolds number on the heat and mass transfer coefficients, heat flux and mass flux across
the polymer hollow fibre module were analysed. Experimentally derived non-dimensional heat and
mass transfer correlations were compared with other correlations from literature. Due to the spindle
shape of proposed hollow fibre module, the shielding with hollow fibre bundles could be avoided
greatly, therefore the mass transfer performance of the proposed system demonstrated significant
improvement compared with other devices reported in literature.

Key words: Polymer hollow fibre, evaporative cooling, heat transfer, mass transfer, experiment

Nomenclature

\( A \) Heat transfer area (m\(^2\))

\( C_p \) Specific heat (kJ/kg K)

\( d \) Fiber diameter (m)

\( h \) Heat transfer coefficient (W/m\(^2\)K)

\( h_v \) Enthalpy of saturated water vapour (kJ/kg);

\( k \) Mass transfer coefficient (m/s)

\( L \) Characteristic length of hollow fibre bundle (m)

\( m \) Mass flow rate (kg/s)

\( n \) Number of fibres inside the heat exchanger

\( N \) Mass flux (mg/m\(^2\) s)

\( Nu \) Nusselt number

\( Pr \) Prandtl number

\( q \) Heat flux (W/ m\(^2\))
Re Reynolds number

Sh Sherwood number

Sc Schmidt number

T Temperature (°C)

U Overall heat transfer coefficient (W/m²K)

V Volumetric flow rate of the incoming air, m³/h;

Q Sensible cooling capacity (W)

Greek Letters/Subscripts

α Air

dew Dew point

dry Dry bulb

e Evaporated water

φ Packing fraction of the module

ε Effectiveness

H Heat transfer

λ Thermal conductivity (W/mK)

M Mass transfer

ρ Density of the fluid (kg/m³)

u Incoming air velocity, m/s

ν Dynamic viscosity of the fluid (kg/ms)
1. Introduction

Global energy demand is soaring during past few decades due to the rapid worldwide economy development and urban sprawl. According to the research report produced by International Institute of Refrigeration, air conditioning system accounts for 45% of the total energy consumption for domestic and commercial buildings[1]. Overall, air-conditioning system takes up approximately 15% of the total energy consumption around the world[1]. In the Middle East, where the climatic condition is dry and humid, air conditioning system consumes as high as 70% of energy required for buildings and around 30% of the total energy[2]. With the impact of global warming, the demands of effective air-conditioning system which consumes less energy and provide higher cooling performance is massive.

The current widely-used vapour compression system plays dominant role in the market. However, vapour compression system has the disadvantages of intensive energy consumption and low performance in hot and humid climate. Moreover, the possible leakage of high GWP refrigerants will lead to the depletion of Ozone Layer, which further contributes to the global warming and other associated environmental and social changes. Hence, the development of more energy efficient and environmental benign cooling systems remains to be the research topics for scientific researches.

In the past few decades, evaporative cooling system arouses great attentions among the researchers due to the fact that it is more environmentally friendly (use of the water as working fluids), simple in structure configuration, and less consumption in primary energy. Direct evaporative cooling system works under the following principle: the incoming hot and humid air gets direct contact with the circulating water, causing the evaporation of the water and the air temperature will be reduced accordingly. Consequently, the evaporated water, in the form of vapour will be absorbed by the air, which leads to the humidity increase of the outlet air.
Recently, the research interests of this topic are focused on pad incorporated evaporative cooling system[3-6], desiccant based evaporative cooling system[7, 8], and dew point based evaporative cooling system[9-12]. Due to the large contact surface area, porous pad incorporated evaporative cooling systems have attracted more attentions. Wu et al.[13] presented a simplified mathematical model to describe the heat and moisture transfer between water and air in a direct evaporative cooler, with pad thickness of 125mm and 260mm, the cooling efficiency reached 58% and 90% respectively. Franco et al. [14] studied the influence of water and air flows on the performance of cellulose media. The results showed that with a thickness of 85mm, a plastic grid pad could offer a cooling efficiency of 65% at wind speed of 1.5m/s. However, since water is directly in contact with the incoming air in the closed system, there is the potential for microbial growth due to the supply of stagnant water. This may provide an opportunity for the spread of liquid phase-born bacterial diseases for occupants[15].

In order to solve this problem, a hollow fibre integrated evaporative cooling system has been proposed. Compared with porous pad media, hollow fibre materials provide several advantages as follows: 1) allow selective permeation of moisture: with pore sizes less than 0.1µm, hollow fibre material will allow the water vapour transfer but eliminate the bacteria and fungi penetration[16]; 2) provide large surface area per unit volume[17], which is favourable for enhanced heat and mass transfer. Detailed descriptions about hollow fiber materials and their applications are summarized in the literature[18]. According to Chen et al.[19], the overall heat transfer coefficients could reach 1675W/m²K with a fibre diameter of 550µm. Kachhwaha and Preahhakar[20] analysed heat and mass transfer performance for a direct evaporative cooler using a thin plastic plate. The experimental testing results indicated that the outlet air temperatures were between 21°C and 23°C, at the inlet dry bulb temperature of 24.8-28.4°C, the air humidity ratio of 2.3-5.8g/kg and air mass flow rate of 0.13, 0.2, 0.3 and 0.4g/s. Zhang[21] proposed the theoretical investigations on a rectangular cross-flow hollow fibre membrane module for air humidification. With 2600 fibres (fibre outside diameter 1.5mm) inside the module, the outlet air temperature could reach 21.5°C when the inlet dry bulb temperature was 30°C. Johnson et al.[15] studied the heat and mass transfer of a hollow fibre membrane evaporative cooling system. With a different range of fibre bundles (9, 19, 29 fibre bundles), the heat transfer area was in the range of
0.35m²-1.13m², and around 0.4°C temperature drop could be observed from the experiments. The above publications are mainly concentrated on the theoretical analysis on the polymer hollow fibre integrated evaporative cooling system. The available experimental results were limited to the variation of outlet air temperatures with respect to different air flow rates. In addition, as stated by Johnson et al.[15], due to the shielding from adjacent fibres, the heat and mass transfer performance will decrease when using a large number of fibres inside one module.

A summary of the recent experimental and modelling works on evaporative cooling system is presented in Table 1. Literature review indicates that the previous published papers were mainly concentrated on the theoretically modelling of evaporative cooling system. For the limited experimental investigations reported in the literature, the evaporative coolers were mainly made from porous paper materials. This paper presents a novel evaporative cooling system with a hollow fibre evaporative cooler. Instead of previously reported cross flow configurations[13, 15, 21], five fibre bundles (each contains 100 fibres) with the distance of 5cm were placed normal to the air stream, with detailed configuration shown in Figure 2. In order to avoid the flow channelling or shielding of adjacent fibres, the fibres inside each bundle were made into a spindle shape to allow maximum contact between the air stream and the fibre. As a subsequent work of previous research[22], this research work extends the previous experimental testing conditions to a wider range, with the incoming air temperature up to 39°C and relative humidity up to 40%. The variations of outlet air dry bulb temperature, wet bulb effectiveness, dew point effectiveness and cooling capacity were studied by varying the incoming air dry bulb temperature from 27°C to 39°C and RH from 23% to 40%. The effects of various incoming air Reynolds number on the heat and mass transfer coefficients, heat flux and mass flux across the polymer hollow fibre module were analysed. Two sets of experimentally derived non-dimensional heat and mass transfer correlations were summarized, which could be favourable for the future design of polymer hollow fibre integrated evaporative cooling system.

2. Heat and mass transfer of hollow fibre evaporative cooling system
The 3D model of the hollow fiber module is shown in Figure 1 together with the temperature and humidity change profile. As illustrated in Figure 1, the incoming hot and humid air gets in contact with the porous hollow fiber module, inside which the water will be circulating around. As water evaporates through the hollow fibers, it will extract energy from the incoming air causing the temperature to drop. As reported by Johnson et al. [15], the resistance of fiber materials is very small, therefore it could be neglected. According to Rawangkul et al. [5],

The sensible cooling capacity \( Q_s \) supplied by the incoming air of such novel evaporative cooling system can be calculated by:

\[
Q_s = m_a C_p \alpha (T_1 - T_2) = \frac{C_p m_a \rho V (T_1 - T_2)}{3.6}
\]

Eq.(1)

Where, \( Q_s \) is the flow of transferred heat (W);

\( m_a \) is the mass flow rate of the incoming air (kg/h);

\( C_p \alpha \) is the specific heat of air at constant pressure, kJ/(kg K);

\( T_1 \) is the dry bulb temperature of the incoming air (°C);

\( T_2 \) is the dry bulb temperature of the outgoing air (°C);

\( \rho \) is the density of the air, kg/m\(^3\);

\( V \) is the volumetric flow rate of the incoming air, m\(^3\)/h;

The rate of water evaporation is:

\[
m_e = m_a (\omega_2 - \omega_1)
\]

Eq.(2)

Where \( m_e \) is the flow of evaporated water (kg/h);
\( m_a \) is the mass flow rate of the incoming air (kg/h);

\( \omega_1 \) is the humidity ratio of the incoming air;

\( \omega_2 \) is the humidity ratio of the outgoing air.

The rate of heat transfer \((Q)\) and the rate of water evaporation \((m_e)\) can be given as the product of heat transfer coefficient and the mean logarithmic difference in temperature \((\Delta T)\), and the product of the mass transfer coefficient and the mean logarithmic difference in the water vapour density \((\Delta \rho_v)\). These can be expressed in the following two equations:

\[
Q = h_H A_s \Delta T = q A_s \quad \text{Eq.(3)}
\]

\[
m_e = h_M A_s \Delta \rho_v = N A_s \quad \text{Eq.(4)}
\]

Where \( h_H \) is the coefficient of heat transfer \((\text{W/m}^2\text{K})\);

\( h_M \) is the coefficient of mass transfer \((\text{W/m}^2\text{K})\);

\( q \) is the heat flux \((\text{W/m}^2)\);

\( N \) is the mass flux \((\text{mg/m}^2\text{s})\);

\( A_s \) is the total surface area of the polymer hollow fibre \((\text{m}^2)\);

The mean logarithmic difference in temperature \((\Delta T)\) and water vapour density \((\Delta \rho_v)\) can be calculated using following equations:

\[
\Delta T = \frac{(T_2 - T_1)}{\ln(\frac{T_2 - T_{wb}}{T_1 - T_{wb}})} \quad \text{Eq.(5)}
\]

\[
\Delta \rho_v = \frac{(\rho v_2 - \rho v_1)}{\ln(\frac{\rho v_2 - \rho v_{wb}}{\rho v_1 - \rho v_{wb}})} \quad \text{Eq.(6)}
\]
Where $\rho_{v1}$ and $\rho_{v2}$ are the water vapour density on entering and leaving the hollow fibres (kg/m$^3$);

$\rho_{wb}$ is the saturated water vapour density at the wet bulb temperature (kg/m$^3$).

The heat and mass transfer coefficients could be calculated from:

$$h_H = \frac{Nu \cdot k}{d_h} \quad \text{Eq.}(7)$$

$$h_M = \frac{Sh \cdot D_{AB}}{d_h} \quad \text{Eq.}(8)$$

Where $k$ is the thermal conductivity of the air (W/mK);

$d_h$ is the hydraulic diameter of the hollow fibre module, m. According to [23], $d_h$ can be calculated as:

$$d_h = \frac{4 \text{ cross sectional area of flow}}{\text{wetted perimeter}} \quad \text{Eq.} \ (9)$$

According to the hollow fiber bundle configuration [24], $d_h$ can further be expressed as:

$$d_h = \frac{4 A_{\text{flow}}}{\pi d_0 + \pi D} = \frac{(1-\varphi)D^2}{\pi d_0 + D} \quad \text{Eq.} \ (10)$$

Where $\varphi$ is the packing fraction of the module;

$d_0$ is the outer diameter of a single fiber;

$D$ is the diameter of the module shell (m);

The relationship between Reynolds number ($Re$), Prandtl number ($Pr$) and Nusselt number ($Nu$), and the relationship between Reynolds number ($Re$), Schmidt number ($Sc$) and Sherwood number ($Sh$) can be expressed by:

$$Nu = C_1 Re^{m_1} Pr^{1/3} \quad \text{Eq.}(11)$$
\[ Sh = C_2 Re^{m_2} Sc^{1/3} \]  
Eq.(12)

Where \( C_1, C_2, m_1, m_2 \) are constants for the hollow fibre bundles.

Reynolds number can be calculated by:

\[ Re = \frac{u d_h}{v} \]  
Eq.(13)

Where \( u \) is the incoming air velocity, m/s;

\( v \) is the viscosity of the incoming air, m²/s.

From the previous study [22], using the experimental data, general empirical correlations for the non-dimensional heat and mass transfer data for the proposed system are derived using mathematical data regression techniques. In this research, as the experimental testing conditions are extended to a large range, the applicability of these equations will be verified in section 4.

\[ Sh = 1.275 Re^{1/3} Sc^{1/3} \]  
Eq. (14)[22]

\[ Nu = 0.958 Re^{1/3} Pr^{1/3} \]  
Eq. (15)[22]

The wet bulb effectiveness (\( \varepsilon_{wb} \)) is an important expression used to characterise the air saturation capacity of the polymer hollow fibre bundle. This is defined as the ratio between the thermal difference on passing through the hollow fibre bundle (\( T_1 - T_2 \)) and the maximum thermal difference that would occur if the air were saturated (\( T_1 - T_{wb} \)):

\[ \varepsilon_{wb} = \frac{T_1 - T_2}{T_1 - T_{wb}} \]  
Eq.(16)

Similarly, the dew point effectiveness (\( \varepsilon_{dew} \)) is defined as the ratio between the incoming air and the outgoing air to the difference between the incoming air and its dew point temperature, as indicated by the following expression:

\[ \varepsilon_{dew} = \frac{T_1 - T_2}{T_1 - T_{dew}} \]  
Eq.(17)

3. Experimental testing rig
A lab scale experimental testing rig is developed, which integrates the hollow fiber evaporative cooler with the evaporative cooling system. Polyvinylidene fluoride (PVDF) hollow fibres (manufactured by ZENA Ltd.) with outside diameter of 0.8mm and inside diameter of 0.6mm, an effective pore size of 0.5µm and a porosity of 50% were used for the fabrication of the polymer hollow fibre module. The polymer hollow fibre module consists of 5 fibre bundles (each contains 100 fibres), which were connected at each bundle ends using T piece plastic tubing. The hollow fibre module was incorporated into a circular aluminium tunnel, whose cross section diameter was 0.15m. In order to avoid the flow channelling or shielding of adjacent fibres, the fibres in each bundle were compressed from both ends to make the bundle into a spindle shape to allow maximum contact between the air stream and the fibres. The detailed physical properties of the polymer hollow fibre module were summarized in Table 2.

The testing rig consists of a polymer hollow fibre module, an air tunnel, a water pump, a fan and a water tank. The detailed schematic diagram is shown in Figure 2. A 5-litre water tank was used to provide water circulation inside the fibre. In order to avoid any particle blockage within the polymer hollow fibres, a water filter was allocated to improve the purity of the incoming water into the fibres. A flow meter and a ball valve were included in the water circulation cycle with the aim to control the water flow rate inside the fibre. In order to minimize the experimental testing errors, four humidity and temperature sensors (EK-H4, Sensirion, UK) were located at the inlet (point 1 in Figure 2) and outlet (point 2 in Figure 2) of the tunnel respectively, to measure the inlet and outlet conditions of the air stream. Additional K type thermocouples were used to measure the water temperature entering and leaving the hollow fibre module (point 3 and 4 in Figure 2). The aluminium tunnel was connected with a variable frequency drive centrifugal fan, which was linked directly with the environmental chamber. The experimental prototype image is shown in Figure 3. The basic working principle of the experiment is as following: The hot and humid air from the environmental chamber will be blown out by the blower into the air tunnel. With the help of the circulation pump, water is circulating from the water tank into the hollow fibre bundles to ensure that the fiber surface will get wetted throughout the tests. The incoming hot and humid air will get in contact with the hollow fibre module. As water evaporates...
through the porous hollow fibres, the temperature of incoming air will be reduced, accompanied by the increased relative humidity.

At the beginning of each test, the environmental chamber was set to the required temperature and humidity level. As soon as the temperature and humidity reached the desired values, the water pump for the fibre module and the fan in the air stream direction was switched on. The air velocity was measured at the five different positions along the cross sections of the outlet aluminium tunnel, using the air velocity probes connected to a recorder (Testo 454). The dynamic pressures in the upstream and downstream of the air flow were recorded using Pressure transducers (Ge UNIK 5000).

For each test, the temperature and humidity values were recorded every 20 seconds until the time when the system reach steady states as indicated by the humidity and temperature sensor readings. The accuracy of the measuring instruments used was: ±0.2% for temperature, ±0.5% for pressure, ±2% for air velocity, and ±2% for relative humidity.

4. Results and discussion

As indicated in Table 3, the experiments were carried out for the proposed novel evaporative cooling system with various inlet air dry bulb temperatures (27°C, 30°C, 33°C, 36°C and 39°C), and various inlet air relative humidity (23%, 32% and 40%). Figure 4 presents the variation of outlet air dry bulb temperatures with respect to various inlet air dry bulb temperatures under different incoming air relative humidity. For incoming air temperature in the range of 27-39°C and the incoming air relative humidity varying from 23%, 32% to 40%, it can be observed that the outlet air temperature is dramatically affected by inlet air relative humidity at constant incoming air temperature. At the same inlet air dry bulb temperature, the higher incoming air relative humidity will lead to the lower outlet air dry bulb temperature. For instance, at the inlet air dry bulb temperature of 30°C, the outlet air dry bulb temperature were 24.8°C, 25.7°C and 26.4°C respectively for RH of 23%, 32% and 40%. This shows that the proposed novel evaporative cooling system has great potential to be used in hot and dry climatic conditions. On the other hand, Figure 4 shows that the outlet air dry bulb temperature tends to form a linear relationship with the inlet air dry bulb temperature at the same inlet air relative
humidity. The slopes of the outlet air dry bulb temperature at constant relative humidity are in the range of 0.7-0.74. This means that, when increasing the inlet air temperature by 10°C, the outlet air temperature will be improved by 7-7.4°C.

Figure 4 also compares the proposed experimental testing data with the outlet dry bulb temperature presented by Dohnal, et al [25], for a compact bundle of 600 polypropylene hollow fibres placed horizontally down the air stream, with the inlet air dry bulb temperature of 24.6°C, and the RH= 25%. It can be found that the presented experimental results agrees well and even shows better cooling performance compared with the testing results obtained by Dohnal et al [25]. This might be due to the fact that the proposed evaporative cooling system adopted the novelty of using spindle shape fibre bundles to allow maximum contact between the air stream and the fibre. While in the experiments proposed by Dohnal et al. [25], the shielding from adjacent fibre in the entire bundles resulted in decreased heat transfer performance.

The wet bulb effectiveness of the proposed novel evaporative cooling system is illustrated in Figure 5. It can be found that, with the incoming air dry bulb temperature in the range of 27-39°C, and RH of 23%, 32% and 40%, the wet bulb effectiveness varies from 0.32-0.45. Higher inlet air dry bulb temperature leads to greater wet bulb effectiveness, due to the fact that larger temperature depression is obtained for higher inlet air temperature. In addition, lower inlet air relative humidity will result in higher wet bulb effectiveness. The reason is due to the fact that drier incoming air with small relative humidity actually represents larger driving force of vapour pressure difference between the inlet and outlet air condition. Thus the drier incoming air can potentially absorb more moisture during the water evaporation process. Therefore, more latent heat will be required during the water evaporation process. Consequentially, a larger amount of sensible heat of the processed air will be transferred from the incoming dry air to the outgoing wet air. This leads to a much lower outlet air temperature compared with air of higher incoming relative humidity. Comparable value of wet bulb effectiveness obtained by Dohnal et al. [25] is also included in Figure 5. With the inlet air dry bulb temperature of 24.6°C, and the RH= 25%, the wet bulb effectiveness achieved by Dohnal, et al. [25] was 0.354, which showed a good agreement with the presented experimental results.
Figure 6 illustrates the variations of dew point effectiveness with respect to different inlet air conditions. When air inlet dry bulb temperature increases from 27°C to 39°C, the dew point effectiveness is in the range of 0.18-0.3. At the same inlet air RH, higher inlet air temperature leads to higher dew point effectiveness, due to the fact that larger temperature depression is obtained for higher inlet air temperature. Moreover, when the inlet air dry bulb temperature maintains at the same level, lower inlet RH will result in higher dew point effectiveness. The reason is similar to what we present in last paragraph, as drier incoming air with smaller relative humidity actually represents larger driving force of vapour pressure, thus leads to higher cooling performance. The dew point effectiveness obtained in this experimental study is slightly better than the results achieved by Dohnal et al. [25], due to the fact that the at lower air velocity, the individual fibres within the bundles were shielded from the air stream, as the majority of the air will go past the outer layer of the fibre bundles. Therefore, such intra-bundle shielding effect in Dohnal et al. [25]’s testing configurations might lead to reduced heat transfer performance.

Figure 7 depicts the variations of cooling capacity with respect to various inlet air dry bulb temperatures under different incoming air relative humidity. Generally, the cooling capacity increases with the improvement of the inlet air dry bulb temperature from 27°C to 39°C. With the same inlet air dry bulb temperature, lower inlet air RH will lead to higher cooling capacity. For instance, when inlet air dry bulb temperature is fixed at 30°C, the cooling capacities are 125.2W, 109.9W and 83.1W respectively for the inlet air RH equals to 23%, 32% and 40%. The reason is due to the fact that, as shown in Eq. (1), the cooling capacity is proportional related to the differences between the inlet air and outlet air dry bulb temperature. Drier incoming air with small relative humidity actually represents larger driving force of vapour pressure difference between the inlet and outlet air condition. Thus the drier incoming air can potentially absorb more moisture, which leads to a much lower outlet air temperature compared with air of higher incoming relative humidity. Therefore, the cooling capacity shows decreased trend when increasing the inlet air RH from 23% to 32% and 40%.

Figure 8 shows the experimental obtained heat flux under different incoming air relative humidity. It can be observed that the heat flux will increase with the improvement of incoming air Reynolds
number. At the same Reynolds number, lower inlet air relative humidity will lead to greater heat flux.

For instance, at Reynolds number of 100, the heat flux increases from 798W to 1512W respectively for RH equals to 40% and 23%. This means that approximately 1.8 times more heat is transferred in the process when RH decreased from 40% to 23%. The reason is because, as shown in Eq. (3), the heat flux is positively related to the inlet and outlet air dry bulb temperature difference. Moreover, as shown in Figure 5, lower inlet air relative humidity will yield much lower outlet air dry bulb temperature, which means greater inlet and outlet air dry bulb temperature difference. This will consequentially lead to higher heat flux. Similar trend could be found in Figure 9, showing the variations of mass flux with respect to Reynolds number under different incoming air RH. It is obvious that higher Reynolds number will contribute to greater mass flux under the same RH. While for the same Reynolds number, lower RH will lead to higher mass flux.

Experimental determined overall heat transfer coefficient ($h_\text{u}$) and mass transfer coefficients ($h_M$) with respect to Reynolds number under different inlet air relative humidity are illustrated in Figure 10 and Figure 11. An increase in Reynolds number yields better heat and mass transfer between the air stream and the water inside polymer hollow fibre. Despite of different inlet air relative humidity, $h_\text{u}$ follows the same linear relationship with Reynolds number, with variations less than 4.1% during the experiments. The similar linear relationship between Reynolds number and $h_M$ is illustrated in Figure 11. Further inspection of Figure 10 and Figure 11 indicate that, by increasing Reynolds number from 0 to 220, $h_\text{u}$ changes from around 60 W/m²K to 250 W/m²K (about 4.2 times), while $h_M$ improves from 0.01m/s to 0.25m/s respectively (about 2.5 times). This indicates the changes of Reynolds number has more significant impact on the heat transfer coefficients than the mass transfer coefficients for the proposed polymer hollow fibre integrated evaporative cooling system.

Figure 12 and Figure 13 respectively illustrated the non-dimensional heat and mass transfer data. It is evident that the three different testing conditions yield more or less the same linear relationship between the logarithm value of $\text{Sh}/\text{Sc}^{1/3}$, $\text{Nu}/\text{Pr}^{1/3}$ and logarithm value of Reynolds number.
The heat and mass transfer data are correlated by an empirical equation as shown in Eq. (11)-(12). The Reynolds number exponent, $\alpha$, in the Eq. (11)-(12) is an indication of the flow conditions. For example, $\alpha=1/3$ indicates laminar flow with fully developed velocity profile. According to literature[26], for $\alpha=0.5$, the indication is for developing velocity and concentration profiles, which is in the entry region condition[27]. For $\alpha$ approaching 0.8-1.0, the flow is in the turbulent flow regime.

For the proposed novel evaporative cooling integrated hollow fibre system, the low Reynolds number (less than 300) clearly shows the laminar flow regime. Therefore, the exponent $\alpha$, for this study will be chosen as $1/3$.

After obtaining the heat and mass transfer coefficients $h_H$ and $h_M$, based on Eq. (7) and Eq. (8), $Nu$ and $Sh$ number can be calculated accordingly. Reynolds number can be obtained by inserting experimental measured air velocity and hydraulic diameter of the hollow fiber module into Eq. (13). $Pr$ number of is taken as 0.713 under the air temperature of 20\degree C. Based on the experimental obtained data, general empirical correlations for the non-dimensional heat and mass transfer data of the proposed system are derived using mathematical data regression techniques:

$$Sh = 1.134 Re^{1/3} Sc^{1/3}$$ Eq. (18)  
$$Nu = 0.976 Re^{1/3} Pr^{1/3}$$ Eq. (19)

The above experimental determined correlation for the non-dimensional heat and mass transfer data of the polymer hollow fibre integrated evaporative cooling system are compared with the results (Eq. (20) and Eq. (14)- (15) obtained by Yang and Cussler[28] and X. Chen et al.[22]. Data from Yang and Cussler[28] and X. Chen et al.[22]'s experiments showed that the exponent of Reynolds number were both equal to 1/3, while the constant for heat transfer correlations were 1.38 and 1.275 respectively. The deviation of the constants for Eq. (18) and Eq.(20) is 21.7%. This is due to the fact that Yang and Cussler[28]'s experimental testing rig contained 750 fibers (outside diameter 0.4mm) inside the module for a liquid-gas heat and mass transfer process, while in the proposed system the fiber number is reduced to 500 with larger
outside diameter of 0.8mm. Such difference in testing configurations could lead to the
discrepancy between the two constants in the equations. On the other hand, different from the
subsequent work of previous research[22], the present work offers a wider range of testing
conditions, for inlet air temperature and relative humidity up to 39°C and 40%. However, the
deviations of the two heat transfer constants and mass transfer constants for the present research
and the previous study are very small, with only 12.3% and 2.1%, as indicated in Eq. (18)-(19)
and Eq. (14)-(15). Such deviations could be due to the unavoidable experimental errors. For
instance, performing the uncertainty analysis proposed by Moffat[29] for Equation (13), the
obtained uncertainty of the Reynolds number is 5.3%. Therefore, it can concluded that for a
wider range of testing conditions, the obtained heat and mass transfer correlations actually
agree well with the previous research[22]. This further proves that the testing conditions do not
have significant effects on the non-dimensional heat and mass transfer data.

\[ Sh = 1.38Re^{0.4}Sc^{1/3} \]  
Eq. (20)[28]

Experimental obtained mass transfer data in comparison with other correlations from literature is
presented in Figure 14. Different groups of mass transfer correlations developed by Zhukauska[30],
Yang and Cussler[28], Cote et al.[31], Chen et al.[22] and Johnson et al.[15] were used to perform the
comparisons. The results obtained from the proposed novel evaporative cooling system is similar to
Cote et al.[31]’s correlation, where the fibre bundle was used to transport oxygen through water. The
presented results are also very close to Johnson et al.[15]’s correlation, which was obtained from the
fibre array integrated evaporative cooler. It is also possible to observe that the mass transfer data for the
present research agrees relatively well with those obtained from the previous research[22]. Furthermore,
Figure 14 demonstrated that the mass transfer performance for the fibre bundles (29 fibres included)
achieved by Johnson et al.[15] are the worst compared with other fibre configurations. In the present
study, the fibre module consists of 5 fibre bundles which contain 100 fibres individually. However, the
mass transfer performance of such proposed fibre module shows significantly improvement compared
with the mass transfer conditions of fibre bundles presented by Johnson et al. [15]. The reason is due to
the fact that, the spindle shape in the proposed system helps to avoid any over-shielding effect within the fibre bundle. By compressing the fibre from both ends, the loosed spindle shape fibre bundle could be obtained, which helps to enable better heat and mass transfer between each individual fibre and the incoming air. For normal shape fibre bundle, such shielding effect is more significant at lower Reynolds number, when the air will go past the outside of the fibre bundle, leaving the majority of the fibre inside the bundle with very little contact with the incoming air. As the Reynolds number increases, better contact between the fibres inside the bundle could be achieved, which leads to better mass transfer performance, as shown in Figure 14.

5. Conclusions

A novel evaporative cooling system with hollow fiber bundles in the spindle shapes is proposed in this research. With the aim to avoid the flow channelling or shielding of adjacent fibres, the fibres were compressed into a spindle shape to allow maximum contact between the incoming air and the fibres. This novel hollow fibre integrated evaporative cooling system will provide a comfortable indoor environment for hot and dry area. Under various inlet air dry bulb temperatures (27°C, 30°C, 33°C, 36°C and 39°C), and various inlet air relative humidity (23%, 32% and 40%), the cooling performances of the proposed novel evaporative cooling system were experimentally investigated. The variations of outlet air dry bulb temperature, wet bulb effectiveness, dew point effectiveness and cooling capacity were studied by varying the incoming air dry bulb temperature. Some conclusions can be found:

1) Increase the inlet air dry bulb temperature will lead to the increase of the outlet air dry bulb temperature, cooling capacity, wet bulb effectiveness and dew point effectiveness. By keeping the inlet air dry bulb temperature at constant value, increase the inlet air relative humidity will lead to the decrease of cooling capacity, wet bulb effectiveness and dew point effectiveness;

2) The heat and mass transfer coefficients remain to be in linear relationships with respect to the Reynolds number, despite of various inlet air relative humidity. With the Reynolds number in the range of 10-220, the heat and mass transfer coefficients were in the range of 50-250W/m²K.
and 0.05-0.3 m/s. Two sets of non-dimensional heat and mass transfer correlations with respect to Reynolds number were deviated from the experimental results, which showed good agreements with other correlations from literature;

3) With inlet air dry bulb temperature being the same, increase the inlet air relative humidity will lead to the decrease of heat flux and mass flux. With the inlet air relative humidity being equal, increase the Reynolds number of incoming air will lead to the increase of heat flux and mass flux;

4) Experimental obtained mass transfer data are illustrated and compared with other correlations from literature. Due to the spindle shape hollow fibre module, the shielding with hollow fibre bundles could be avoided greatly, therefore the mass transfer performance of the proposed system demonstrated significant improvement compared with other devices reported in literature. The non-dimensional heat and mass transfer data comparisons indicate that the variations of experimental testing conditions have very limited impact on the heat and mass transfer correlations.

5) The wet bulb effectiveness achieved in the proposed research was between 0.3 and 0.45 with the packing fraction of 0.028. In the literature, the packing fraction was 0.28 in Zhang [21], which was about 10 times higher than what the hollow fiber module presented in this paper. However, the cooling effectiveness was only 1.5-2 times higher than that is obtained in this research. This means that the design of this hollow fiber integrated evaporative cooler prototype could provide comparably cooling performance as presented by other researchers, but with lower packing fraction factor (fewer fibers included). The future work could be concentrated on increase the packing fraction by inserting more fibers into the one bundle, in order to potentially increase the cooling effectiveness.

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### Table 1 Summary of some published research results on evaporative cooling systems

| Reference     | Research method                  | Evaporative cooler type/materials               | Inlet air temperature (°C) | Outlet air temperature (°C) | Wet bulb effectiveness | Conclusions                                                                 |
|---------------|----------------------------------|------------------------------------------------|-----------------------------|----------------------------|------------------------|-----------------------------------------------------------------------------|
| Wu et al. [13]| Simulation (simplified model)    | Direct evaporative cooler/Porous honeycomb paper | 27-37                       | 23-28                      | 0.6-1.0                | 1) Frontal air velocity and pad thickness of the module are two key factors for the evaporative cooling system. 2) The optimum frontal velocity was 2.5m/s |
| Lin et al. [32]| Experiment + Simulation (ε-NTU method) | Dew point evaporative cooler/ hydrophobic material | 22-30                       | 25-18                      | 0.6-1.0                | 1) The saturation point of the working air is influenced by the working air ratio and channel height; 2) Overall heat transfer coefficient could achieve higher than 100W/m²K |
| Zhang [33]     | Experiment + Simulation (fractal theory) | Direct evaporative cooler/hollow fiber membrane | NA                          | NA                         | NA                     | 1) Experimental obtained relationship between Sherwood and Reynolds number was established using fractal model; 2) Membrane module with higher packing fraction could lead to better heat transfer performance. |
| Franco et al. [14] | Simulation                  | Direct evaporative cooler/ Porous paper           | NA                          | NA                         | 0.6-0.8                | 1) Comparisons of the cooling performance of five different porous materials revealed that the plastic grid block produced highest efficiency of 82.6%; 2) Higher efficiency will lead to lower specific water consumption |
| Zhao et al. [34]| Simulation                     | Dew point evaporative cooler/ Porous polygonal stack | 28°C                        | NA                         | 0.5-1.3                | 1) Cooling effectiveness increased with the increase of the working-to-intake air ratio; 2) Under UK summer design condition, the wet-bulb and dew-point effectiveness could reach up to 1.3 and 0.9. |
Table 2 Geometric and physical properties of the polymer hollow fibre evaporative cooler

| Property                              | Symbol | Values | Unit  |
|---------------------------------------|--------|--------|-------|
| Duct cross section diameter           |        | 0.15   | m     |
| **Duct total length**                 | L      | 0.9    | m     |
| Fibre number inside the module        | N      | 5*100=500 (5 bundles) |       |
| Fibre outside diameter                | \(d_o\) | 0.8    | mm    |
| Fibre inside diameter                 | \(d_i\) | 0.6    | mm    |
| Nominal pore size                     |        | 0.2    | µm    |
| Fibre porosity                        |        | 0.6    |       |
| Packing density                       |        | 10.67  | \(m^2/m^3\) |
| Packing fraction                      | \(\varphi\) | 0.028  |       |
| Polymer hollow fibre thermal conductivity | k    | 0.17   | W/mK  |

Table 3 Testing conditions of the novel polymer hollow fiber integrated evaporative cooling system

| Property                              | Symbol | Values | Unit |
|---------------------------------------|--------|--------|------|
| Incoming air velocity                 | \(v_a\) | 0.1-5.0 | m/s  |
| Water flow rate inside fibre          |        | 0.05   | l/m  |
| Incoming air temperature              | \(T_a\) | 27-39  | ºC   |
| Incoming air humidity                 | \(RH\) | 23-40  | %    |
Figures

Figure 1 The 3-D model and the temperature and humidity change profile in the hollow fibre module.

Figure 2 Schematic diagram of polymer hollow fibre integrated evaporative cooling system.
Figure 3 Testing rig of polymer hollow fibre integrated evaporative cooling system.

Outlet Air Dry bulb Temperature (°C) vs. Inlet Air dry bulb Temperature (°C) for different RH levels:
- RH=23%
- RH=40%
- RH=32%

T_{in}=24.6°C, RH=25% (Dohnal, et al, 2012)
Figure 4: Variations of outlet air dry bulb temperatures with respect to various inlet air dry bulb temperatures under different incoming air relative humidity ($u=4.6m/s$)

Figure 5: Variations of wet bulb effectiveness with respect to various inlet air dry bulb temperatures under different incoming air relative humidity ($u=4.6m/s$)

Figure 6: Variations of dew point effectiveness with respect to various inlet air dry bulb temperatures under different incoming air relative humidity ($u=4.6m/s$)
Figure 7 Variations of cooling capacity with respect to various inlet air dry bulb temperatures under different incoming air relative humidity.

Figure 8 Variations of heat flux with respect to Reynolds number under different incoming air relative humidity.
Figure 9 Variations of mass flux with respect to Reynolds number under different incoming air relative humidity.

Figure 10 Variations of heat transfer coefficients with respect to Reynolds number under different incoming air relative humidity.
Figure 11 Variations of mass transfer coefficients with respect to Reynolds number under different incoming air relative humidity

Figure 12 Variations of Non-dimensional heat transfer data under different incoming air relative humidity
Figure 13 Variations of Non-dimensional mass transfer data under different incoming air relative humidity

Figure 14 Comparisons of mass transfer data of presented results with other correlations in literature

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607 Lists of Figures

Figure 1 Temperature and water vapour profiles in polymer hollow fibre integrated evaporative cooling system

Figure 2 Schematic diagram of polymer hollow fibre integrated evaporative cooling system

Figure 3 The 3-D model (A) and the actual prototype image (B) of the hollow fibre module

Figure 4 Testing rig of hollow fibre integrated evaporative cooling system

Figure 5 Variations of outlet air dry bulb temperatures with respect to various inlet air dry bulb temperatures under different incoming air relative humidity

Figure 6 Variations of wet bulb effectiveness with respect to various inlet air dry bulb temperatures under different incoming air relative humidity
Figure 7 Variations of dew point effectiveness with respect to various inlet air dry bulb temperatures under different incoming air relative humidity

Figure 8 Variations of cooling capacity with respect to various inlet air dry bulb temperatures under different incoming air relative humidity

Figure 9 Variations of heat transfer coefficients with respect to Reynolds number under different incoming air relative humidity

Figure 10 Variations of mass transfer coefficients with respect to Reynolds number under different incoming air relative humidity

Figure 11 Variations of Non-dimensional heat transfer data under different incoming air relative humidity

Figure 12 Variations of Non-dimensional mass transfer data under different incoming air relative humidity

Figure 13 Variations of heat flux with respect to Reynolds number under different incoming air relative humidity

Figure 14 Variations of mass flux with respect to Reynolds number under different incoming air relative humidity

Figure 15 Comparisons of mass transfer data of presented results with other correlations in literature

List of Table

Table 1 Physical properties of the polymer hollow fibre module