Broadband and Broad-Angle Low-Scattering Metasurface Based on Hybrid Optimization Algorithm

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A broadband and broad-angle low-scattering metasurface is designed, fabricated, and characterized. Based on the optimization algorithm and far-field scattering pattern analysis, we propose a rapid and efficient method to design metasurfaces, which avoids the large amount of time-consuming electromagnetic simulations. Full-wave simulation and measurement results show that the proposed metasurface is insensitive to the polarization of incident waves, and presents good scattering-reduction properties for oblique incident waves.

Metamaterials are engineered materials with unusual constitutive parameters such as negative permittivity and permeability. They are usually composed by periodic resonant or non-resonant units with the characteristic dimensions much smaller than the wavelength. One important application of the metamaterials is to achieve electromagnetic invisibility or transparency, which can greatly reduce the radar cross section (RCS) of metallic or dielectric targets. The approach of optical transformation provides an efficient way to bend the incident waves along the boundary of a region to be hidden without perturbing the exterior fields. Therefore perfect invisibility can be achieved with no backward or forward RCS. However, the objects inside are completely isolated, which makes such devices hindered in practical applications. Another promising method is based on the scattering cancellation, where metasurface has been utilized to wrap the objects, and it can provide additional surface reactance in order to generate anti-phase scattered fields. But the bandwidth of the metasurface is usually very limited. The radar absorbing material can also be used for RCS reduction, which transforms electromagnetic energy into heat. But the change of the object temperature will inevitably increase the detection possibility by infrared detectors.

In this paper, we develop a low RCS metasurface using the windmill-shaped unit. The phase of each unit is chosen to be distributed randomly. The reflected waves from each part of the metasurface will experience destructive interference due to the random phase difference, leading to electromagnetic diffusion for the scattering waves. The design of the proposed metasurface seems to be the counterpart of the traditional reflectarray, which requires the reflected waves to be steered over a range of directions. In order to redistribute the scattering energy into all the directions, a large phase swing (i.e., the available phase shift of the composing unit) is usually required, while the magnitude of the normalized reflection efficient for the unit is kept to approach zero (dB) at the same time. Similar techniques for RCS conduction based on the objects’ coating have been reported in Refs. [15–17], where both the perfect conductor and artificial magnetic conductor (AMC) have been used to create a chessboard-like structure. The reflected waves from the two units have 180 phase difference, hence the destructive interference between the two waves will dramatically reduce the scattering field level. The bandwidth of such coating is also restricted since it is usually hard to design broadband AMC structures. The mechanism of the proposed metasurface mainly depends on the random distribution of the reflection phases, which is totally different from the mechanisms mentioned above.

Results
Metasurface is a two-dimensional equivalent of three-dimension metamaterial (see Fig. 1), which could be used to control the reflection and transmission properties for the incident waves, and therefore achieve some interesting functionalities such as focusing and wave bending. Usually a metasurface is composed by periodic or aperiodic elements, which are printed on the surface of a thin substrate.
For a metasurface composed by large number of units with the same type and different geometrical dimensions, electromagnetic dif-
fusions will be caused, resulting in low backward RCS26. However, it is usu-
ally hard to simulate the far-field scattering radiation pattern due to the
burden of computation time and memory sources. Therefore the
optimization of such metasurface for RCS reduction becomes very
inefficient and impractical based on the simulation results. Actually
the scattering pattern of such complex array can be rapidly synthe-
sized when the mutual coupling between the adjacent elements are
achieved through simple numerical simulations27–28. Let us consider a
two dimensional metasurface composed by M*N units. When illu-
nimated by a plane wave, the total scattering wave from the meta-
surface can be regarded as the superposition of the scattering wave from
each basic element, which can be expressed as follows,

\[ E_{\text{total}} = \sum_{m=1}^{M} \sum_{n=1}^{N} E_{m,n}(0, \phi) e^{i\phi_{m,n}} \]  

(1)

where \( E_{m,n} \) is the vectorial far-field scattered by the element \([m,n]\). \( 0 \) and \( \phi \) are the polar and, azimuthal angle, respectively. To obtain
the scattering field of each element, the infinite periodic array model is
adapted to calculate the coefficient \( E_{m,n} \) in Eq. (1). We assume that
every element is surrounded by the same cells when considering the
influence of mutual coupling. This is an approximate model which
does not correspond to the realistic metasurface configurations.

Here the induced surface currents from each element with peri-
odic boundaries can be extracted from the numerical simulations.
Take a small metasurface of 5*5 units for example, (as shown in
Fig. 1(a)), the metallic windmill-shaped structure is selected as the
basic element, and a perfect conductor layer is attached to the back of
the substrate. From the equivalence principle, there are three kinds
basic element, and a perfect conductor layer is attached to the back of
the substrate. From the equivalence principle, there are three kinds
of equivalent current on the surface of each element: the equivalent
current, the magnetic current, and the electric current. The infinite peri-
dodic boundaries can be extracted from the numerical simulations.

In our simulation, the full-wave electromagnetic simulation tool FEKO
is used to extract the equivalent currents mentioned above. When the
metasurface is illuminated by a plane wave, the scattering field of
each element can be written as

\[ E(r) = L_c[I_c] + L_d[J_d] + L_d[M_d] \]  

(2)

where

\[ L_c[I_c] = -j\omega A_c - \nabla \phi_c \]

\[ = \frac{j\omega}{4\pi} \left\{ \int_{\text{conductors}} I_c(r') G(r : r') ds' \right\} \left\{ \nabla \int_{\text{conductor}} \rho_c(r') G(r : r') ds' \right\} \]  

(3)

\[ = \frac{1}{j\omega} \left\{ \int_{\text{conductors}} I_c(r') G(r : r') ds' + \nabla \int_{\text{conductor}} \nabla' J_c(r') G(r : r') ds' \right\} \]

and

\[ L_d[J_d] = -j\omega A_d - \nabla \phi_d \]  

(4)

\[ L_d[M_d] = - \frac{1}{\varepsilon_0} \nabla \times F \]  

(5)

where

\[ A = \frac{\mu}{4\pi} \int_{\text{dielectric}} J_d(r') G(r : r') ds' \]  

(6)

\[ \phi = - \frac{1}{4\pi\varepsilon_0} \int_{\text{dielectric}} \nabla' J_d(r') G(r : r') ds' \]  

(7)

\[ F = \frac{\varepsilon}{4\pi} \int_{\text{dielectric}} M_d(r') G(r : r') ds' \]  

(8)

and \( G(r : r') \) is the green function in free space.

Here the dimension of example is 60 mm × 60 mm, with several
random-sized windmill-shaped structures. The radiation pattern the
metasurface in Fig. 2(a) is also simulated by FEKO to check the
agreement between the synthesis method and the numerical method,
as shown by the black line and the red line in Fig. 2(b). It is clear that
the synthesis method in Eq. (1) provides satisfactory prediction of the
scattering pattern of the metasurface from the comparison. There are
some discrepancies in the sidelobes from the two results in Fig. 2(b),
which is mainly due to the mismatch of the boundary conditions
used in the simulations. From the comparison between the simulated
and synthesized radiation pattern, both results agree well which
means that this model sufficiently provides a powerful means for
radiation pattern prediction and optimization.

To get best performance of the metasurface, a particle swarm
optimization (PSO) algorithm is utilized together with far-field pat-
tern prediction to achieve the optimal arrangement of the meta-
atoms. In PSO algorithm every particle can be seen as an individual
who searches for the optimum solution through cooperation in indi-
viduals and sharing information, which is an intelligent optimization
algorithm proposed by Kenndey and Eberhart31. It has been widely
applied to the optimization of various electromagnetic problems due
to the merits like simple principle, few parameters and fast conver-
gence. The potential solution can be deemed to a particle, whose
mathematical description of the speed and location of next genera-
tion could be expressed as,

\[ v_{ik}^{t+1} = \omega v_{ik}^t + c_1 \times \text{rand}_1 \times (p_{best}^t - x_{ik}^t) + c_2 \times \text{rand}_2 \times (g_{best}^t - x_{ik}^t) \]  

(9)

\[ x_{ik}^{t+1} = x_{ik}^t + v_{ik}^{t+1} \]  

(10)

Where \( \omega \) is the inertia coefficient, \( c_1 \) and \( c_2 \) are the acceleration
constants, which are used to adjust individual speed. \( \text{rand}_1 \) and \( \text{rand}_2 \) are random numbers between 0 and 1. \( p_{best}^t \) is the individual
optimal location, \( g_{best}^t \) is the global optimal location. In the design of
metasurface, \( x \) denotes the size of basic unit, and the performance
of metasurface is evaluated by \( \text{fitness}(x) \), which is described as,

\[ \text{fitness} = c_3 \times \max(\text{E}_d) + c_4 \times \text{E}_{s,t} \]  

(11)

where \( c_3 \) and \( c_4 \) refer to weight coefficients. E_d denotes the total
scattered field, E_{s,t} denotes scattered field in the specific direction.
Such fitness function aims at reducing the scattering energy mostly in
the direction of maximum radiation.

**Figure 1 | Reflection and transmission of electromagnetic waves on the metasurface.**
The design flow of the low RCS metasurface is shown in Fig. 3, where two modules have been used to get the desired optimal design. The PSO module evaluates the fitness, updates the particle speed and the population location (i.e. the meta-atom arrangements) in each iteration, and then sends the information to the far-field scattering pattern module. The latter gives the scattering pattern of the optimized metasurface based on the equivalent currents mentioned in last sections and calculates the reduction of RCS in the main scattering directions. Then the value of fitness is computed and returned to PSO module. After some iterations, we can get the optimal arrangement of metasurface with lowest RCS as required. The kernel of this flowchart is that the PSO module determines various combinations of basic unit, whose performances are judged by the far-field pattern analysis module to find the best solution.

A low RCS metasurface is designed, as shown in Fig. 4(a). The windmill shaped structure is selected to be the basic element. It is composed by an inner square ring and an outer irregular ring, and their resonance frequencies are designed to be very close in order to increase the operation bandwidth and the reflection phasing range. The curves of the reflection phase from 6 GHz to 14 GHz is almost linear, and they are nearly parallel with the change of L (the length of the branch of the outer ring), showing excellent broadband frequency response as required\[32\]. Here we choose the dimensions of the basic element in Fig. 4(a) as \(a=12 \text{ mm}, \ g=0.4 \text{ mm}, \ d=0.55 \text{ mm}, \ h=4 \text{ mm}\). The substrate used in the simulation and experiment is F4B (\(\varepsilon_r=2.65 +0.001\)) with the thickness 4 mm. The reflection phase of the basic element is extracted through the numerical simulations with the change of L at 8 GHz, 10 GHz, 12 GHz and 14 GHz (see...
These curves are nearly parallel with each other, showing excellent linear frequency response, which is critical to guarantee the working bandwidth. It is clear that a large phasing range can be achieved when tuning the branch of the outer ring, which is important to ensure the performance of the low RCS metasurface.

In this design, for the simplicity of optimization, we choose elements with discrete phase distributions instead of continuous ones as mentioned above. Here eight windmill-shaped elements with different dimensions have been selected as the composing unit of the metasurface. When the length of the branch \( L \) is 0.6 mm, 0.825 mm, 1.05 mm, 1.26 mm, 1.47 mm, 1.75 mm, 2.05 mm and 2.38 mm respectively, the reflected phase is \( 45^\circ n \) (\( n = 1 \) to 8) degrees at the central frequency \( f = 10 \) GHz, as illustrated in Fig. 4(b).

The whole metasurface is made up of 144 windmill-shaped units, and we need to find the optimal combination for the desired low RCS metasurface based on the eight basic elements. In our algorithm, a population size of 400 and a maximum of 100 iterations are predefined. It will take 9 hours to finish the every iteration based on the numerical simulation. However, the time spent in every iteration using the far-field scattering module is approximately 10 minutes.

Figure 4 | (a) Basic element of the low RCS metasurface and the layout of the designed metasurface, (b) the reflection phase from 6 GHz to 14 GHz with the change of \( L \) in Fig. 4(a), (c) the reflection phase at different frequency with the change of \( L \).

Figure 5 | (a) Far-field scattering pattern (\( \vartheta = 0^\circ \)) from numerical simulation (by FEKO) and far-field scattering pattern analysis, (b) simulated RCS reduction for normal incidence from 6 GHz to 14 GHz.
with the same hardware, which is much more efficient than before. After some iterations, the arrangement of the basic elements is finally determined with the layout shown in Fig. 4(a).

Fig. 5(a) shows the scattering pattern of the metasurface from full-wave simulations and far-field pattern prediction analysis. Both results seem to agree very well, which validates the whole design flow in Sec. 3. The RCS reduction for a bare metallic plate and the designed metasurface at different frequencies is illustrated in Fig. 5(b), where the RCS reduction is greater than 10 dB from 7 GHz to 13 GHz.

Discussion
In order to verify the theoretical analysis above, a larger metasurface containing 16 by 16 units, optimized by the algorithm, has been fabricated and tested, as depicted in Fig. 6. The transmitting and receiving horn antennas have been connected to a vector network analyzer (Agilent N5230C) to measure the RCS of the metasurface.

The simulated and measured RCS reductions for vertical and horizontal polarizations are shown in Figs. 6(c)(d) and Figs. 6(e)(f) respectively. The maximal RCS reduction can be found to exceed 30 dB as we can see from the measured results. The metasurface shows excellent broadband properties, where the RCS reduction is over 10 dB from 7 GHz to 14 GHz. With the increase of the incident angle, the bandwidth decreases a little due to the phase aberrations. Similarly, the maximum of RCS reduction is also decreased. However, low RCS properties are still kept for the proposed metasurface.
We have proposed the design algorithm for a low RCS metasurface with ultra-low backward scattering. The optimization method is used together with the far-field scattering pattern technique to find the desired broadband metasurface. The simulated and measured results demonstrate that the metasurface can effectively decrease the backward scattering from 7 GHz to 14 GHz, which is important for stealth applications in the future.

**Methods**

The sample is placed as high as the horn antennas in the experiment. The distance $R$ (3 m) between antennas and sample is chosen far enough to avoid the near field effect. Pyramidal absorbing materials have been placed around the sample to decrease the unwanted reflections from the surroundings. In addition, a copper plate with the same size has also been measured for comparison. In the case of normal incidence, the transmitting and receiving horn antennas are placed adjacent, where the real incident angle is about 3 degree because of the restricted size of horn antennas. Both the transmitting and receiving horn antennas can move along the circumference trace to obtain RCS reductions at different scattering angle $\theta_{scatt}$, where we only consider the case that the scattering angle $\theta_{scatt}$ equals to the incident angle $\theta_{inc}$.

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**Author contributions**

Q.C. and T.J.C. conceived the idea. K.W. did the theoretical calculations and designed the samples. K.W., J.Z. and D.S.D. performed the measurements. K.W. and Q.C. wrote the manuscript based on input from all authors. All authors contributed to the discussions.

**Additional information**

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