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The formation of magnetic depletions and flux annihilation due to reconnection in the heliosheath

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**ABSTRACT**

The misalignment of the solar rotation axis and the magnetic axis of the Sun produces a periodic reversal of the Parker spiral magnetic field and the sectored solar wind. The compression of the sectors is expected to lead to reconnection in the heliosheath (HS). We present particle-in-cell simulations of the sectored HS that reflect the plasma environment along the Voyager 1 and 2 trajectories, specifically including unequal positive and negative azimuthal magnetic flux as seen in the Voyager data ([Burlaga et al. 2003](https://doi.org/10.1051/0004-6361:20031046)). Reconnection proceeds on individual current sheets until islands on adjacent current layers merge. At late time bands of the dominant flux survive, separated by bands of deep magnetic field depletion. The ambient plasma pressure supports the strong magnetic pressure variation so that pressure is anti-correlated with magnetic field strength. There is little variation in the magnetic field direction across the boundaries of the magnetic depressions. At irregular intervals within the magnetic depressions are long-lived pairs of magnetic islands where the magnetic field direction reverses so that spacecraft data would reveal sharp magnetic field depressions with only occasional crossings with jumps in magnetic field direction. This is typical of the magnetic field data from the Voyager spacecraft ([Burlaga & Ness 2011](https://doi.org/10.1073/pnas.1021088108), [Burlaga et al. 2016](https://doi.org/10.1002/2015JA021644)). Voyager 2 data reveals that fluctuations in the density and magnetic field strength are anti-correlated in the sector zone as expected from reconnection but not in unipolar regions. The consequence of the annihilation of subdominant flux is a sharp reduction in the “number of sectors” and a loss in magnetic flux as documented from the Voyager 1 magnetic field and flow data ([Richardson et al. 2013](https://doi.org/10.1073/pnas.1215706110)).
1. INTRODUCTION

The rotation of the Sun twists the solar dipole field into the dominant azimuthal Parker spiral magnetic field $B_T$ separated by the heliospheric current sheet. Because of the misalignment of the solar rotation axis and magnetic axis the current sheet flaps in the vertical direction as it propagates outward from the Sun, producing the sectored magnetic field (Wilcox & Ness 1965) in which azimuthal magnetic field $B_T$ reverses sign around every 13 days (the RTN coordinate system is defined with R in the radial direction, T in the azimuthal direction with positive T in the direction of the Sun’s rotation and N, which points North in the equatorial plane, completes the triad). The sector-zone occupies a latitudinal extent that varies during the solar cycle, reaching nearly the poles when the fields from the Sun are a maximum (Smith 2001).

An important question is whether the sectored magnetic field can reconnect to release magnetic energy and accelerate particles. In the solar wind around 1AU the heliospheric current only occasionally undergoes reconnection (Gosling 2007), probably because the current sheet is far wider than the characteristic ion inertial scale $d_i = c/\omega_{pi}$ (where collisionless reconnection onsets) (Cassak et al. 2005). As a result, the sector structure of the solar magnetic field survives out to the termination shock (TS) even though the periodicity of the current sheet becomes increasingly irregular with distance from the Sun (Burlaga et al. 2003, 2005, 2006). It has been suggested that the drop in the solar wind density with distance and therefore the increase in $d_i$, combined with the compression of the current sheets downstream of the TS, leads to the onset of reconnection in the sectored heliosheath (HS). Such reconnection has been proposed as a source of free energy to drive the production of anomalous cosmic rays (ACRs) (Drake et al. 2010; Opher et al. 2011) and as a source of turbulence in the heliosheath that might control the transport of energetic particles (Burgess et al. 2016). The reduction of the plasma flow in the HS on its approach to the heliopause is expected to further compress the sectored magnetic field, inevitably leading to the onset of reconnection in the HS (Czechowski et al. 2010; Drake et al. 2010; Opher et al. 2011; Borovikov et al. 2011). However, determining the thickness of the heliospheric current sheets downstream of the TS to confirm that collisionless reconnection should onset in the HS is a challenge because of the low and variable speed of plasma flows in the HS and because weak magnetic fields there are difficult to measure. It has been suggested that current sheets in the HS are thicker than the ion inertial scale (Burlaga & Ness 2011) but post reconnection final states are characterized by magnetic islands in which current layers are comparable in width to
the island width. Thick current sheets might therefore suggest that reconnection in HS has already taken place.

In any case, smoking gun evidence from the Voyager observations that reconnection in the sectored HS has taken place has not been identified. The challenge is that the Voyager magnetometers were not designed to measure the weak magnetic fields in the outer heliosphere (∼ 0.1nT with noise levels ∼ 0.05nT) and Voyager 1 has no plasma measurements. Further, the dynamics of reconnection in the high β environment of the HS remains relatively poorly understood (Schoeffler et al. 2011, Schoeffler et al. 2013) compared with the typically β ∼ 1 conditions at 1AU. The multiple sharp dropouts of energetic particles of heliospheric origin measured by Voyager 1 at the HP boundary (Stone et al. 2013) do suggest the existence of magnetic islands and therefore magnetic reconnection at and in the vicinity of the HP (Swisdak et al. 2013; Strumik et al. 2013, 2014).

There are a variety of indirect indicators that reconnection is active in the HS, including the loss in magnetic flux documented by Voyager 1 (Richardson et al. 2013) and the dropouts in the “low energy” electrons at Voyager 2 (Opher et al. 2011; Hill et al. 2014). In the absence of reconnection the azimuthal magnetic flux $V_R R B_T$ is preserved in the heliosphere in regions where the flow is dominantly radial. While Voyager 1 was in the HS, the radial flow $V_R$ dropped essentially to zero (Krimigis et al. 2011) while there was no significant increase in $B_T$. A significant flow in the N direction (to the North in the case of Voyager 1) might convect the flux away and therefore prevent the pileup of $B_T$. However, the Voyager 1 data suggested that $V_N$ was also very small (Decker et al. 2012; Stone & Cummings 2012). Thus, it seems likely that reconnection must be playing a role in the Voyager 1 flux loss measurements. On the other hand, reconnection actually does not normally reduce the magnetic flux in a reconnecting current layer. Rather, the flux that reconnects at an x-line is convected into the adjacent magnetic island such that the integrated magnetic flux is preserved (Fermo et al. 2010). The flux loss issue can therefore not be simply resolved by invoking reconnection without a more careful analysis. The dropouts in low energy electrons at Voyager 2 were attributed to Voyager 2 leaving the sector zone (Opher et al. 2011; Hill et al. 2014). The argument was that electrons can rapidly escape from a region of the heliosheath with laminar (unreconnected) magnetic fields while reconnected magnetic fields and associated magnetic islands would be more effective in suppressing electron transport along the ambient magnetic field. Thus, higher electron fluxes in the sectored heliosheath are evidence that the heliosheath magnetic field had reconnected – in the absence of reconnection there is no reason that the transport properties of the sectored and non-sectored HS should differ.

The Voyager observations in the HS have uncovered other issues related to the reconnection or not of the sectored magnetic field. The first concerns the polarity of the
HS magnetic field. The nominal polarity of the magnetic field in the Northern hemisphere during the time period 2000-2011 is negative (corresponding to the azimuthal angle $\lambda = \arctan(B_T/B_R) = 90^\circ$) \cite{Burlaga & Ness 2012, Richardson et al. 2016}. When Voyager 1 is in the sector zone, $\lambda$ typically flips back and forth between $90^\circ$ and $270^\circ$ and a long period of $90^\circ$, which occurred in 2011, would normally be interpreted as an excursion out of the sector zone and into the unipolar zone. On the other hand, the MHD models of the global heliosphere predict that the sector zone should be convected to the North as the HS plasma approaches the HP so that Voyager 1 should remain within that sector zone prior to its crossing of the HP \cite{Opher et al. 2011, Borovikov et al. 2011}. Similarly, in 2011-2012 Voyager 2 saw significantly fewer excursions into negative (North latitude polarity) than expected based on the Wilcox Solar Observatory predictions \cite{Richardson et al. 2016}. Why the Voyagers are seeing fewer excursions into magnetic field polarities that are opposite to their heliolatitude is a mystery.

A second mystery concerns the distinct magnetic structures seen in the Voyager 1 and 2 data. At “proton boundary layers (PBLs)” the magnetic field strength either rises or drops by factors of up to three with no measurable change in the azimuthal angle $\lambda$ or the elevation angle $\delta = \arcsin(B_N/B)$ (the angle of the magnetic field with respect to the R-T plane) \cite{Burlaga & Ness 2011, Burlaga & Ness 2012}. Since these regions of magnetic field enhancement or depletion can last for days, it seems unlikely that they are associated with kinetic scale instabilities such as mirror modes, which typically produce localized “humps” in the magnetic field rather than depletions in high $\beta$ plasma \cite{Baumg"artel et al. 2003}.

Here we address the dynamics of reconnection in the sectored HS with the goal of understanding the signatures and consequences of the reconnection and the resultant structure of the HS magnetic field. The simulations extend earlier models by considering more realistic initial conditions that account for unequal positive and negative azimuthal magnetic flux. That the sector zone does not carry equal positive and negative flux at the latitudes of the Voyager spacecraft trajectories is evident from the Voyager observations in the solar wind in the outer heliosphere but upstream of the termination shock \cite{Burlaga et al. 2003}. In this region because the solar wind velocity greatly exceeds the spacecraft velocity, time in a region of given polarity is linked to the integrated magnetic flux in a given sector. The Voyager data in the high-speed solar wind of the outer heliosphere reveals that sector spacing is highly erratic and therefore positive and negative fluxes are unequal. For the time period 2000-2011 one might expect that for Voyager 1 the negative polarity dominates because the spacecraft is closer to the Northern boundary of the sector zone, which has negative polarity, while for Voyager 2 positive polarity dominates. Unequal magnetic fluxes were required to reproduce Voyager 1 magnetic data in MHD simulations of reconnection at the HP \cite{Strumik et al. 2014}.
The consequence of unequal fluxes is profound. At late time when reconnection is nearly complete, bands of single polarity flux survive, which tends to organize the sector structure more than in earlier simulations in which magnetic islands dominated the magnetic structure at late time (Drake et al. 2010; Opher et al. 2011). The simulations are also carried out with high initial $\beta$ and with initial force-free current layers rather than Harris type current layers, which are typically not seen even at 1AU (Smith 2001). Because of the high $\beta$ the magnetic field at late time exhibits large-scale depletions in which the magnetic field strength drops by around a factor of three over a narrow boundary layer with little variation in the direction of the magnetic field. The plasma density and temperature rise slightly within the depletions to maintain pressure balance. The radial width of these magnetic depletions is around three times the width of the initial sector with the subdominant magnetic flux. The depth of these depletions and their widths (when normalized to the initial separation of current layers) are universal values that are linked to the intrinsic properties of collisionless magnetic reconnection. The boundaries of these magnetic depletions exhibit a striking resemblance to the “proton boundary layers” seen in the Voyager data. We show that reconnection on adjacent current layers conspires to completely annihilate the subdominant magnetic flux, leading to regions of unipolar flux. Pairs of magnetic islands do survive at late time although the volume of plasma associated with these remnant islands is small compared with the regions of magnetic depletion. The island structures exhibit magnetic dips and rotations in the magnetic field direction that might be interpreted as sector crossings in satellite data. The simulations therefore offer a possible explanation of the predominance of unipolar flux and the loss of magnetic flux seen in the Voyager 1 magnetic field data. Finally, analysis of the Voyager 2 magnetic field and plasma data reveals that fluctuations in magnetic field strength and density are anti-correlated in the sectored HS, as expected from reconnection, but not in the unipolar HS. As a whole, the consistency of the Voyager data with unique reconnection signatures establishes with high likelihood that reconnection in the sectored HS has taken place.

2. PIC model and initial conditions

We carry out 2-D particle-in-cell (PIC) simulations of the sector structure in the $x−y$ plane of the simulation, which maps to the heliospheric $R−T$ plane. The simulations are performed with the PIC code p3d (Zeiler et al. 2002) using a periodic equilibrium magnetic
field

\[
\frac{B_y}{B_0} = \tanh \left( \frac{x - 0.2L_x}{w_0} \right) - \tanh \left( \frac{x - 0.3L_x}{w_0} \right) + \tanh \left( \frac{x - 0.7L_x}{w_0} \right) - \tanh \left( \frac{x - 0.8L_x}{w_0} \right) - 1.
\]  

(1)

For this magnetic configuration there are four current layers centered at \(x/d_i = 20.48, 30.72, 70.68\) and \(81.92\) on a computational domain that is \(L_y \times L_x = 409.6 \times 102.4\) where lengths are expressed in units of \(d_i = c_A/\Omega_i\) the proton inertial length. The total magnetic flux in the positive \(y\) direction is four times that in the negative \(y\) direction. The initial plasma density \(n_0\) and temperatures \(T_e\) and \(T_i\) are constants and the out-of-plane magnetic field \(B_2^z = B_0^2 - B_0^z\) is chosen to produce force balance. This initial state is not a rigorous kinetic equilibrium, especially for ions, but does not display unusual behavior at early time. The results are presented in normalized units: the magnetic field to the asymptotic value of the reversed field \(B_0\), the density to \(n_0\), velocities to the proton Alfvén speed \(c_A = B_0/\sqrt{4\pi m_in_0}\), times to the inverse proton cyclotron frequency, \(\Omega_i^{-1} = m_ic/eB_0n_0\), and temperatures to \(m_ic_A^2\). We define some additional scale lengths as follows: \(w_0 = 0.25d_i\) is the half-width of an individual current sheet and \(\Delta_x = \Delta_y = 0.05d_i\) are the grid scales. To maximize the separation between the macroscales \(L_x\) and \(L_y\) and the kinetic scales, we choose a modest ion to electron mass ratio of 25 and velocity of light \(c\) of \(15c_A\). The particle temperatures are initially uniform with \(T_i = 5.0m_ic_A^2\) and \(T_e = 2.0m_ic_A^2\) so \(\beta = 8\pi n_0(T_e + T_i)/B_0^2 = 14\) is large, as expected for the heliosheath. The average number of particles per cell is 100. Reconnection begins from particle noise.

The overall scale sizes of our simulations are much smaller than those of the heliospheric sectored field. The widths of the sectors upstream of the TS are around \(1.7 \times 10^8\) km, which at a density of \(0.001/cm^3\), is around \(2 \times 10^4d_i\). Compression across the shock and the approach to the heliopause reduces the sector width somewhat but the sector spacing continues to be far larger in units of \(d_i\) than the values we can implement in our simulations. However, we have shown earlier that the rate of growth of islands is insensitive to the kinetic scale \(d_i\) (Schoeffler et al. 2012) and the same conclusion applies to the simulations presented here. Thus, the reconnection rates and associated bulk ion flows can be translated to the heliosheath by normalizing to the Alfvén speed and the Alfvén transit time \(L_x/c_A\).

3. Simulation results

In Fig. 1 we show 2D plots of the magnetic field strength \(B\) and the magnetic field lines around the two lower current layers in the system at times \(\Omega_i t = 50, 200\) and 350. The
initial magnetic field points to the left above and below the two current layers and to the right between the two layers. In (a) and (b) a large number of very small islands grow on the two current layers at early time. These islands coalesce and continue to grow until in (c) and (d) they span the entire region between the adjacent current layers. At this point all of the magnetic field lines spanning the simulation domain in the positive y direction have reconnected. On the other hand, positive magnetic flux still exists. Along a single cut in x in (d) $B_y$ has positive and negative values. However, island merging and reconnection continues and at later time in (e) and (f) much of the positive magnetic flux has been annihilated. How this happens is important first because of the flux loss documented by the Voyager 1 observations and second because magnetic reconnection normally preserves the magnetic flux. At the magnetic x-line field lines reconnect but the integrated unsigned flux through a magnetic island is unchanged as reconnection proceeds. Namely, there is no flux loss at the center of the island and magnetic flux is preserved elsewhere so the total magnetic flux contained in an island is preserved. On the other hand, it is evident from Fig. 1(f) that on a cut along $x$ at $y \sim 240$ $B_x$ will only have positive values – there is no surviving negative flux in this region.

The pressure anisotropy that develops during magnetic reconnection in a high \( \beta \) system such as the HS weakens the tension force exerted by the magnetic field on the plasma and therefore slows reconnection and allows islands take elongated forms (Drake et al. 2010; Opher et al. 2011; Schoeffler et al. 2011). A video animation of the magnetic field $B$ for the full duration of the simulation domain (up until $\Omega_{ci} t = 440$) is available online. The movie reveals that the evolution of the magnetic field slows dramatically at late time, a consequence of the pressure anisotropy, and allows isolated elongated magnetic islands to survive late in time.

In Fig. 2 we show a blowup of $B$ and associated magnetic field lines at four times to illustrate how flux annihilation in the geometry of the sectored heliosphere takes place. Again, the magnetic field lines above and below the two current layers initially point to the left and between the two current layers point to the right. In (a) magnetic islands on the two current layers do not yet cross-connect with the adjacent current layer and there is positive magnetic flux that spans the domain in $y$. In (b) the magnetic separatrix of the large island on the lower current layer connects with the upper current layer. At this point there is still substantial negative magnetic flux even though there are no positive $B_y$ field lines that span the system along the $y$ direction. However, the positive magnetic field $B_y$ of the island on the lower current layer begins reconnecting with the negative flux above the upper current layer, which annihilates the positive flux. In (d) almost all of the magnetic flux in the island from the lower current layer has been annihilated, eliminating the surviving positive flux.
The late-time ($\Omega_p t = 440$) structure of the magnetic fields, density, and temperature of the full simulation domain are shown in Figs. 3 and 4. In Fig. 3(a) and (b) are $B$ and field lines of the entire $x-y$ computational domain. Surviving at late time are two pairs of islands embedded in a lower and upper band of depleted magnetic energy. Elsewhere the islands have reconnected away, leaving only negative magnetic flux. The structure of the magnetic depletions is further illustrated in cuts of $B$ in (c), $n$ in (d), $T_i$ in (e) and the azimuthal angle $\lambda = \arctan(B_y/B_x)$ in (f), where $\lambda$ defines the direction of the magnetic field in the $x-y$ plane with respect to the $x$ direction. The location of the cut is marked by the white line in Fig. 3a. The cut in Fig. 3a is chosen specifically because it represents what a satellite might typically see in a heliosheath where reconnection has already annihilated significant magnetic flux. The strong depletions of the magnetic field seen in (c) span the region around each pair of adjacent current layers in the initial system and are a consequence of growth and merger of magnetic islands on adjacent current layers. The boundaries of the magnetic depletions mark the maximum spatial extent of reconnection of adjacent current layers. Pressure balance is maintained within the magnetic depletions by small increases in the density and ion temperature. The increase in electron temperature (not shown) is even smaller. In the cut shown here the azimuthal angle $\lambda$ is nearly constant at 270°. In this region all of the initial positive flux has been annihilated. The scale length of the boundaries of the magnetic depletions are expected to scale with the proton Larmor radius $\rho_i$ because the protons carry most of the pressure and they are able to decouple from the magnetic field on scale lengths of the order of several $\rho_i$ (Drake et al. 2009). For the simulation of Fig. 3, the proton Larmor radius is around 2.2$d_i$ so the scale lengths of the boundaries of the magnetic depletions in Fig. 3(c) are $3 - 5\rho_i$. We emphasize that the scale lengths of these boundary layers are insensitive to the initial width of the initial current sheets because the boundaries are associated with the upstream edges of the reconnection exhaust, which is controlled by local physics – ions move from upstream into the exhaust and are accelerated up to the Alfvén speed across a narrow boundary layer (Drake et al. 2009).

Figure 4 is similar to Fig. 3 but the cuts are now taken through the pair of magnetic islands on the top band of depleted magnetic field. Again the white line shows the location of the cut in Fig. 4(a). The centers of the two islands can be seen in Fig. 4(b) but are most evident in the cut of $\lambda$, which jumps sharply from 270° to 90° and back across the centers of the islands. The island centers are locations of minima of $B$ and small peaks in the density and ion temperature. Distinguishing the crossing of such an island from the crossing of the heliospheric current sheet in the heliosheath would be difficult because the traditional signatures of reconnection, such as high-speed flow, have died away – the system has evolved to a quasistatic state. We emphasize that the probability of crossing a region where the subdominant magnetic flux survives at late time in the system is small. In Fig. 4 the spatial
distribution of $\lambda$ at late time is shown in (a) and in (b) is the probability distribution of $\lambda$. The probability of finding $\lambda \sim 90^\circ$ in this simulation at late time is finite but small.

We can give estimates for the widths and size of the magnetic depletions based on how reconnection developed to produce the final states shown in Figs. 3 and 4. The total width of the magnetic depletion can be calculated by determining the spatial extent of reconnection leading to the final state. Consider two adjacent current layers separated by a distance $\delta L$ with a total magnetic flux between the two layers $\delta \psi$. The separatrix magnetic field line that connects to the two x-lines in Fig. 2(b) was originally at the center of the region between the two nearby current layers at $x/d_i = 20$ and 30. Thus, during the reconnection that led to this state half of the magnetic flux in the region between the two current $\delta \psi$ layers reconnected with the flux above the current layer at 30 and half reconnected with the flux below the current layer at 20. Thus, the spatial extent in $x$ of the entire region inside of the reconnected field lines is $2 \delta L$ ($\delta L/2$ above the upper current layer, $\delta L/2$ below the lower current layer and the region $\delta L$ between the two current layers). During the time from Fig. 2(b) to late time the remaining positive flux $\delta \psi/2$ surrounding the island centered at $x \sim 20$ and $y \sim 185$ reconnects with the negative flux above the upper current layer. At the end of this reconnection process the island is gone. The same happens as the positive flux in the island centered at $x \sim 30$ and $y \sim 145$ reconnects with the negative flux below the lower current layer. The reconnection of these two islands with flux above and below extends the reconnection zone another distance $\delta L/2$ above and below the reconnection zone shown in Fig. 2(b). Thus, at the end of the reconnection process the total extension of the reconnection zone is $3 \delta L$. The total surviving magnetic flux over this domain is $\delta \psi$ ($\delta \psi$ each from above and below the initial current layers and $-\delta \psi$ from between the current layers). Since this flux is spread out over a distance that is three times the initial separation of the current layers, the magnetic field strength is $B_0/3$, independent of the size of the simulation domain, current layer separation or plasma parameters. The cuts of $B$ in Fig. 3(c) display depletions with widths that are around 30, consistent with this estimate, and with magnetic field minima that are close to $0.33B_0$. A Probability Distribution Function (pdf) of the magnitude of the in-plane magnetic field $B_{plane}$ is presented in Fig. 4. There are distinct peaks in the pdf at the initial magnetic field strength $B_0$ and at $B_0/3$. Of course, if the disparity between positive and negative flux is insufficient, the magnetic islands growing on all current layers will ultimately overlap and the organized magnetic depletions shown in Figs. 3 and 4 will not characterize the final state. The disparity between positive and negative flux needs to exceed two for the isolated depletions to survive at late time.
4. Observational Results from Voyager 2

Our simulations of the sectored HS suggest that large depletions in the magnetic field result from magnetic reconnection. The “proton boundary layers” (Burlaga & Ness 2011; Burlaga & Ness 2012) that have been identified in the Voyager 1 and 2 data look very much like the boundaries of the strong magnetic depletions that we see in our simulations. Because reconnection-driven flows are Alfvénic and therefore fall below the local magnetosonic velocity in the high-\(\beta\) heliosheath, reconnection dynamics is to lowest order incompressible, which means that depletions in the magnetic field pressure correspond to enhancements in the plasma density and pressure. This can be seen in the cuts across the magnetic depletions in the simulation data presented in Figs. 3 and 4. Thus, if the magnetic field disturbances in the sectored heliosheath are driven by reconnection, they should correspond to perturbations in the density such that deviations of the magnetic field and density from the ambient background are anti-correlated – reductions (increases) of the magnetic strength should correspond to local increases (decreases) in the plasma density. In the non-sectored heliosheath this anti-correlation should not be present unless there are mechanisms for generating non-compressible turbulence other than reconnection.

Thus, we have explored the correlation between magnetic field and density fluctuations in the Voyager 2 datasets. The plasma instrument on Voyager 1 failed many years ago so correlation studies with the Voyager 1 data are not possible. We have compared the fluctuations of the density \((dn)\) and magnetic field magnitude \((dB)\) in a heliosheath region where the sector structure is observed (2008.2 - 2009.15, 344 days of data) with those in a unipolar region (2009.15 -2010.5, 455 days of data) (Burlaga & Ness 2011; Richardson et al. 2016). We use daily averages of the magnetic field magnitudes from the SPDF website and of the density from the MIT Voyager web site. Figure 7 shows histograms of \(\frac{\langle dBdn \rangle}{\sqrt{\langle dB^2 \rangle \langle dn^2 \rangle}}\) where \(dB = B - \langle B \rangle\) and \(dn = n - \langle n \rangle\). The average \(\langle A \rangle\) of any quantity \(A\) is defined over a 25 day averaging window. The histograms are clearly different for the two regions, with \(dB\) and \(dn\) usually having opposite signs (anti-correlated) in the sector region but not in the unipolar region. Thus, the Voyager 2 data suggests that fluctuations in the sectored heliosheath are driven by reconnection. Alternative explanations for the anti-correlation between the fluctuations in the magnetic field intensity and density would need to explain why the fluctuations are anti-correlated in the sectored zone but not in the unipolar region.

To compare this correlation data with that from our simulation, we evaluate

\[
\frac{\delta n \delta B_{\text{plane}}}{\sqrt{\langle \delta n^2 \rangle \langle \delta B_{\text{plane}}^2 \rangle}}
\]
with $\delta f = f - \langle f \rangle$ for any function $f$ and where $\langle f \rangle$ is an average over the simulation domain. The pdf of this correlation is shown in Fig. 8. As in the observational data the density and $B_{\text{plane}}$ are anti-correlated and there is a distinct tail on the negative side of the distribution.

5. Discussion

We have carried out kinetic simulations of magnetic reconnection in the sectored heliosheath that include the asymmetry in the magnetic flux in the sectors that is expected near the Northern and Southern latitude boundaries of the heliospheric sector zone. We show that when the magnetic flux asymmetry is more than a factor of two, bands of unreconnected magnetic flux $B_T$ survive and sandwich bands that have strongly depleted magnetic field. In the final state the widths of the depletion regions are around three times the width of the initial current layer separations with magnetic field strengths that are around one third of the pre-reconnection intensity. The boundaries of the depletion regions are sharp – several times the proton Larmor radius. The reconnection of magnetic islands on adjacent current sheets leads to the nearly complete annihilation of flux in the subdominant direction. Such flux annihilation does not typically take place during magnetic island growth on a single current layer because magnetic islands conserve the integrated magnetic flux. The final state has scattered pairs of remnant magnetic islands in which the subdominant magnetic flux survives. Cuts across these islands would appear like crossings of an undisturbed heliospheric current sheet – the azimuthal angle $\lambda$ jumps sharply from $90^\circ$ to $270^\circ$ and then reverses across the cores of these islands (Fig. 4). The probability of crossing such an island, however, is low compared to that of crossing a pristine region of magnetic depletion (Fig. 3).

In the spherically expanding solar wind the conservation of magnetic flux implies that $V_R B_T R$ is a constant. For a constant solar velocity $V_R$ this expression yields the usual falloff of $B_T$ as $1/R$, which has been documented in the solar wind. In the heliosheath the magnetic field is more complex because of the development of latitudinal flows $V_N$. However, it was a major surprise when the estimated radial plasma flows $V_R$ at the Voyager 1 spacecraft dropped to essentially zero in 2010 (Krimigis et al., 2011) and yet the magnetic field strength did not increase to compensate (Burlaga & Ness, 2012). Since the velocity $V_N$ was also close to zero, the loss of magnetic flux through a flow to high latitude was insufficient to explain the apparent loss of flux. The conclusion therefore was that the Voyager 1 observations documented a flux loss in the heliosheath (Richardson et al., 2013). In contrast, the magnetic field and flow measurements at Voyager 2 suggested that flux was conserved along its trajectory.
The model presented here might explain how magnetic flux could be lost in the sectored heliosheath. Of course, if flux annihilation as discussed here did take place in the heliosheath at the location of Voyager 1, one would expect to see fewer sector crossings than expected in the magnetic field data. From 2010 to the heliopause crossing in mid 2012 the Voyager 1 spacecraft did see less Southern polarity flux than expected from the WSO data. However, during the long period during which the measured value of $V_R$ decreased at Voyager 1, the data does not suggest a reduced probability of Southern polarity magnetic flux. Indeed, there is an unexplained period during 2008–2010 when the probability of seeing Southern polarity flux is much higher than expected (Richardson et al. 2016). Magnetic reconnection nevertheless seems to be the only viable mechanism that can explain the flux loss along the Voyager 1 trajectory.

The challenge is to identify a more direct method of establishing whether reconnection is taking place in the heliosheath. This is not easy because crossing a current sheet where reconnection is actually taking place is highly improbable. There have now been several hundred identifications of active reconnection in the solar wind at 1AU and yet there is not a single documented observation of the crossing of a magnetic x-line where active reconnection is ongoing – how does one distinguish a static current layer from a current layer where reconnection is active? This requires the accurate measurement of the intense Hall electric field that bounds the current layer on either side of the x-line (Drake et al. 2008), which has not been measured in the solar wind. The documented reconnection observations (Gosling et al. 2005; Gosling 2007) are crossings of the reconnection exhaust, where the measured exhaust velocity has been cross-checked with the predictions based on the Walén condition (Hudson 1970). What are the corresponding direct signatures of reconnection in the heliosheath? We have argued previously that if reconnection onsets just downstream of the termination shock, where the heliospheric current sheet should be compressed below the ion inertial scale $d_i$, the growth time for islands to reach the characteristic sector spacing should be around 60 days, which translates to a distance around 2-3 AU downstream of the termination shock (Schoeffler et al. 2012). Deep within the heliosheath the sectors should therefore have reconnected and the signatures of reconnection should reflected in the late-time structure of the magnetic remnants of reconnection rather than an active reconnection site. That reconnection is taking place in the heliosheath is also supported by the ACR spectra, which peak well downstream of the termination shock (Stone et al. 2005; Decker et al. 2005; Decker et al. 2008). Reconnection downstream of the termination shock is one possible explanation of these observations (Drake et al. 2010; Opher et al. 2011). Some more recent theoretical models suggest that reconnection dynamics downstream of the shock is an intrinsic component of the termination shock structure and associated particle acceleration (Zank et al. 2015).
In the core of the sector zone, where the positive and negative polarity fluxes are nearly equal, the late time state consists of elongated magnetic islands \cite{opher2011} while closer to the latitudinal boundaries of the sector zone where positive and negative polarity fluxes are not equal, the spacecraft observations should resemble the cuts shown in Figs. 3 and 4. The magnetic depletions across rather narrow boundary layers, which can extend to several AU in width, are the clearest direct signatures of the post reconnection heliosheath. The “proton boundary layers (PBLs)” that have been documented in the Voyager 1 \cite{burlaga2011, burlaga2012} and 2 \cite{burlaga2016} data are very similar to the magnetic depletions that appear in our simulations. A surprise is that many of the clearest examples of PBLs from the Voyager 1 data seem to have jumps in magnetic field strength that are around three, which is the value which follows from our analysis of the reconnection dynamics. The measured scale lengths of the measured PBLs are $5 - 10 \rho_i$, which are modestly wider than those seen in our simulations. Other suggestions are that the PBLs result from the growth of mirror modes \cite{burlaga2011, burlaga2012}. However, mirror modes tend to take the form of humps rather than depletions in high $\beta$ systems \cite{baumgertel2003} and the overall spatial scale of the depletions from mirror modes are far smaller than the typical depletions measured in the heliosheath. In contrast the size of the depletions from reconnection are not linked to any kinetic scale but to the radial scale length of the sectors, which can be of the order of an AU. The depletions from mirror modes would also require a significant magnetic field component in the $N$ direction so that the elevation angle $\delta$ would be substantial. Large values of $\delta$ that extend over the regions of magnetic field depletion are not typically seen in the spacecraft data.

Finally, intrinsic to reconnection in a high $\beta$ system such as the HS, where the Alfvén speed is well below the magnetosonic speed, is that the dynamics is nearly incompressible so that the magnetic depletions seen in the simulations are supported by corresponding increases in the plasma pressure (and density). Thus, the fluctuations in the magnetic field strength and density from reconnection should be anti-correlated. The data from Voyager 2 confirms the anti-correlation of fluctuations in magnetic field strength and density in the sectored HS but not in the unipolar HS as expected if reconnection is taking place in the sectored HS.

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Fig. 1.— (Color online) The magnetic structure in the lower half of the simulation domain at $\Omega_i t = 50, 200, \text{ and } 350$ during the simulation. The magnetic field $B$ is shown in (a), (c) and (e) and the in-plane field lines are shown in (b), (d) and (f). The magnetic field $B$ from the simulation is available online as a video. The video runs from time zero to $\Omega_i t = 440$ and shows the actual aspect ratio of the lower half of the computational domain.
Fig. 2.— (Color online) A blowup view of the time evolution of a pair of magnetic islands at $\Omega_i t = 100, 150, 200$ and 250 showing how the subdominant flux is annihilated. The magnetic field $B$ is shown in color and the overlaid white lines are magnetic field lines. The times shown are before the islands overlap the adjacent current layer in (a), when they first intersect the adjacent current layer in (b) and when the magnetic flux in the islands is eroded in (c) and (d).
Fig. 3.— (Color online) The late-time ($\Omega, t = 440$) structure of the magnetic field $B$ in (a) and magnetic field lines in (b) over the entire simulation domain. Cuts across the magnetic depletions along the white line in (a) showing $B$ in (c), of the density $n$ in (d), the ion temperature $T_i$ in (e) and the azimuthal angle $\lambda$ in (f).
Fig. 4.— (Color online) The late-time ($\Omega_i t = 440$) structure of the magnetic field $B$ in (a) and magnetic field lines in (b) over the entire simulation domain. Cuts through a remnant pair of magnetic islands along the white line in (a) showing $B$ in (c), of the density $n$ in (d), the ion temperature $T_i$ in (e) and the azimuthal angle $\lambda$ in (f).
Fig. 5.— (Color online) At late time the spatial distribution of the azimuthal angle $\lambda$ in the full simulation domain (a) and its probability distribution in (b). Note the prominence of the dominant magnetic polarity at late time. The ratio probability of dominant to subdominant polarity in the initial state was four.
Fig. 6.— From the simulation at late time the Probability Distribution Function (pdf) of the strength of the in-plane magnetic field $B_{\text{plane}} = \sqrt{B_x^2 + B_y^2}$. Note the distinct peak at $B_0/3$. 
Fig. 7.— Histograms of $\langle dBdn \rangle / \sqrt{\langle dB^2 \rangle \langle dn^2 \rangle}$ where $dB = B - \langle B \rangle$ and $dn = n - \langle n \rangle$ from Voyager 2 in the sectored region (top) and the unipolar region (bottom). We use 25 day averaging windows.
Fig. 8.— From the simulation a histogram of $\delta n \delta B_{\text{plane}} / \sqrt{\langle \delta n^2 \rangle \langle \delta B_{\text{plane}}^2 \rangle}$ where $\delta n = n - \langle n \rangle$, $\delta B_{\text{plane}} = B_{\text{plane}} - \langle B_{\text{plane}} \rangle$ with $n$ the density, $B_{\text{plane}}$ the magnitude of the in-plane magnetic field and $\langle n \rangle$ and $\langle B_{\text{plane}} \rangle$ the average over the computational domain.