Online Multimodal Transportation Planning using Deep Reinforcement Learning

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Abstract—In this paper we propose a Deep Reinforcement Learning approach to solve a multimodal transportation planning problem, in which containers must be assigned to a truck or to trains that will transport them to their destination. While traditional planning methods work “offline” (i.e., they take decisions for a batch of containers before the transportation starts), the proposed approach is “online”, in that it can take decisions for individual containers, while transportation is being executed. Planning transportation online helps to effectively respond to unforeseen events that may affect the original transportation plan, thus supporting companies in lowering transportation costs. We implemented different container selection heuristics within the proposed Deep Reinforcement Learning algorithm and we evaluated its performance for each heuristic using data that simulate a realistic scenario, designed on the basis of a real case study at a logistics company. The experimental results revealed that the proposed method was able to learn effective patterns of container assignment. It outperformed tested competitors in terms of total transportation costs and utilization of train capacity by 20.48% to 55.32% for the cost and by 7.51% to 20.54% for the capacity. Furthermore, it obtained results within 2.7% for the cost and 0.72% for the capacity of the optimal solution generated by an Integer Linear Programming solver in an offline setting.

I. INTRODUCTION

This paper introduces an online planning algorithm that we developed for a logistics company, based on Deep Reinforcement Learning (DRL). One of the crucial challenges faced by the company and other companies like it, is multimodal transportation planning, in which a container must be assigned to a transportation resource for onward transportation.

Fig. 1 shows a simple example of a multimodal transportation planning problem. Given a set of containers, each with its arrival time and due date at destination, and a set of available vehicle options, each with its transportation costs, and arrival/departure time, the goal is to assign each container to one of the available options, in such a way that the total cost is minimized. As trains have a lower cost than trucks, solving the planning problem corresponds to allocating as many containers to trains as possible.

Multimodal transportation involves complex operational processes, each including many operational activities in different organizations such as seaports, airports, logistics companies, train stations, etc. Any delays, operational errors, and so on, in these operational activities can lead to unexpected events such as, for instance, delays in train arrivals or containers arrivals. At the same time, new containers continuously arrive and customers may require unexpected changes to their orders. These unexpected events introduce unpredictable dynamicity in multimodal transportation, which has a strong impact on the extent to which the plan can be executed. Consequently, transportation planners are continuously replanning, while the plan is being executed. Traditional offline planning methods cannot help transportation planners with that task, because these methods assign batch of containers to available vehicles in one go. However, when an unforeseen event happens, the planner needs to replan only a single container or the few containers that are affected by such event. We refer to this as online (re)planning. Currently, there is little support for online planning, usually carried out by means of heuristics whose outputs may be far from the optimal. To fix this gap, in this work we propose an online planning method for multimodal transportation based on DRL. The method is able to learn rules to assign individual containers to available vehicles, while the plan is being executed. To the best of our knowledge, such an approach has not yet been studied in this domain.

We tested our method using data simulating a realistic scenario, designed on the basis of a real case study of multimodal transportation planning at a logistics company. Our results show that our algorithm can learn rules to effectively assign containers to trains and trucks, one container at a time. Furthermore, it outperformed the tested competitors in terms of total transportation costs and utilization of train capacity, generating a solution close to the offline optimal one.

The rest of this paper is organized as follows. Section II introduces relevant related literature. Section III provides a formal definition of the multimodal transportation problem. Section IV introduces our method. Section V discusses our experiments and evaluation results. Finally, Section VI draws conclusions and delineates future works.

II. LITERATURE REVIEW

In this section, first we discuss approaches related to transportation planning in presence of dynamicity. Then, we
discuss Deep Reinforcement Learning (DRL) applications in the operation research area.

A. Multimodal Freight Transportation Planning

Table II categorizes related work on multimodal transportation planning with dynamicity on the basis of the following features: (1) Modality considered (rail/road/air/water), (2) Planning type (offline/online), (3) Planning method, (4) Dynamicity, where “general” stands for methods able to deal with any unexpected event, and “specific” stands for methods considering only specific types of unexpected events, e.g., the train arrival time.

Most of the methods in Table II are offline [1], [2], [4], [5], [6], [7], [8], [9], [10], [11], [12] meaning they assume to have a-priori information about all containers, and plan all containers together. Still, these papers take dynamicity into account to some extent. However, in most cases this is realized by assuming the shipments to have a known probability distribution, then integrating the unexpected events via offline model-driven approaches methods such as stochastic programming or robust optimization. An exception is [3], where they mix data-driven approaches with model-driven stochastic methods. This method is also able to do replanning after any unexpected events for each container separately. To this end, it analyzes the solution structure of a centralized optimization method, which uses offline analysis and classification on historic data to derive online decision-making rules for suitable allocations of containers to inland services. The weak point of this approach is the offline learning phase. This model needs to re-train periodically to learn new patterns. In contrast, our method is able to replan each container individually after any unexpected and can learn patterns and rules of transportation online.

B. Deep Reinforcement Learning Applications in Decision Making and Combinatorial Optimization Problems

One popular application of Reinforcement Learning in transportation optimization area is the Vehicle Routing Problem (VRP). The objective of VRP is minimizing the total route length while satisfying the demand from all customers [13], which is modeled as a Traveling Salesman Problem (TSP) optimization problem. A number of Deep Reinforcement Learning have been proposed to tackle this problem. For example, [14] introduced a transportation Pointer Networks (PtrNet) [15] able to learn a sequence model coupled with an attention mechanism trained to output TSP tours. A few years later, in [16], to train a DNN they use a policy gradient and a variant of the Asynchronous Advantage Actor-Critic (A3C) method, proposed by [17]. The authors of [13] use the Asynchronous Actor-Critic Agents (A3C) algorithm which is provided by [17]. In [18], a structure2vec (S2V) model was trained to output the ordering of partial tours using Deep Q-Learning (DQN). One year after that, [19] proposed a hybrid approach using 2-opt local search on top of tours trained via Policy Gradient. In [20], they extended network consideration using a reinforce method with a greedy rollout baseline. In other recent works, the authors of [21] propose a Deep Reinforcement Learning algorithm trained using Policy Gradient to learn improvement heuristics based on 2-opt moves for the TSP and in [22] they use a hybrid of Deep Reinforcement Learning and local search for the VRP.

Another relevant domain where DRL is often applied, is manufacturing. In [23], they introduce a Deep Reinforcement Learning method in a dynamic manufacturing environment to allocate waiting jobs to available machines/resources. They apply the DQN algorithm and have an agent for each work center. In [24], authors propose a Reinforcement Learning based Assigning Policy (RLAP) method for multi-projects scheduling in cloud manufacturing to minimize both the total makespan and the logistical distance. To minimize the makespan for an MCP scheduling problem, the authors of [25] propose a reinforcement learning (RL) algorithm to setup a change scheduling method. [26] discusses a Reinforcement Learning method to find the optimal trade-off between conflicting performance metrics for the optimization of the total expected profit of the system.

Applications of RL methods in decision making and Combinatorial Optimization Problems (COP) are not limited to VRP or manufacturing area. In [27], RL is used for deriving the optimal ordering of a network in real time bidding systems. In [28], a deep Reinforcement Learning approach using state aggregation is developed for solving knapsack problems in the business field. In the supply-chain domain, [29] authors use a Reinforcement Learning method for a large variable-dimensional inventory management problem, while [30] proposes a Reinforcement Learning based model for adaptive service quality management in E-Commerce websites. This analysis shows that there are other Reinforcement Learning applications for various optimization problems. However, to the best of our knowledge, no previous work proposed to exploit Deep Reinforcement Learning in multimodal transportation planning.

III. PROBLEM DEFINITION

In this section, we provide a formal definition for the multimodal transportation planning problem we aim to solve. We provide two formulations. First, we define the problem in an offline setting, as a classical combinatorial optimization problem. Then, we define the problem in an online setting in the form of a Markov Decision Process (MDP).

A. Offline Planning Problem Definition

We represent the offline multimodal transportation planning problem as a mathematical programming problem. Variables used to model the problem are described in Table III. Given a multimodal transportation problem with containers and transportation resources with their schedule and capacity, the goal is to determine an assignment of containers to available vehicles, such that the total cost of transportation is minimal. Formally, this is expressed by Equation I. This minimization problem has to fulfill the following constraints: (1) each container is assigned to exactly one train or truck (Equation 2). (2) a container should be planned on a train
only if the train departs on or after the earliest availability day of the container (Equation 3). Containers planned on a train should arrive at the latest on their latest arrival day (Equation 4). Consequently, the transportation problem can be defined as:

\[
\text{Minimize } \sum_{i \in I} \sum_{t \in T} C_t \cdot X^t_i + \sum_{i \in I} C \cdot B_i \tag{1}
\]

Subject to:

\[
\sum_{i \in I} X^t_i + B_t = 1, \quad \forall t \in T \tag{2}
\]
\[
X^t_i \cdot d_i \geq X^t_i \cdot e_i, \quad \forall t \in T, i \in I \tag{3}
\]
\[
X^t_i \cdot a_r \geq X^t_i \cdot l_i, \quad \forall t \in T, i \in I \tag{4}
\]
\[
\sum_{i \in I} X^t_i \leq cap_t, \quad \forall t \in T \tag{5}
\]

### B. Online Planning Problem Definition

We represent the online multimodal transportation planning problem as a Markov Decision Process (MDP). In each state of the MDP, some containers have already been assigned and an action must be taken to assign the next container to a transportation resource, leading to a new state in which one or more containers have been assigned. This must be done in such a way that the total (expected) costs of assigning containers to transportation resources is minimized. Consequently, the MDP is defined by the following elements.

The set of states \( S \), where each state has two components. The first component of our states is a list of train capacities, \( \{cap_1, cap_2, \ldots, cap_j\} \), where each \( cap_j \) represents the number of slots available on the train or trains that correspond to a particular train schedule. In particular, \( cap_1 \) represents the number of slots available on the train or trains with (departure day, arrival day at destination) equal to (1,1), \( cap_2 \) is the total capacity available for (departure day, arrival day at destination) equal to (1,2), and so on. As a consequence, the arrival and departure times of trains are implicitly encoded in the state. Note that, if we have multiple trains with the same departure and arrival day, in this way they are part of the same \( cap_j \). The second component of our states is the information about the next container that must be assigned. More precisely, a container \( i \) is represented by the earliest day on which this container is available at the logistics company \( e_i \) and the due delivery day \( l_i \). The next container to assign is selected using a heuristic. Two alternative heuristics are compared as explained further on in this paper.

The set of actions \( A \), consisting of all possible train options \( T \) and an option ‘Truck’ that is assumed to be always available and uncapacitated. Once an action \( a \) is chosen in state \( s \), the next state \( s' \) is determined by reducing the capacity of the selected train by 1, if a train is chosen, and by selecting the next container to plan. Note that not all actions are possible in each state, because of the constraints that apply (see Section II-A). For example, a train could have no more slots available, or its scheduled departure time could not meet the due delivery date of the container.

The reward function \( R(s, a) \), which is the negative cost associated with selecting an action \( a \) (transportation cost of the selected train/truck) from the list of eligible actions:

\[
R(s, a) = \begin{cases} 
- C_a, & a \in T \\
- C, & a = \text{Truck} 
\end{cases} \tag{6}
\]

The objective, which is maximizing the expected cumulative reward of the selected actions. Note that this is equal to minimizing the expected cumulative cost of transportation. We use the Bellman equation [34] to calculate this.

### IV. DEEP REINFORCEMENT LEARNING FOR SOLVING ONLINE PLANNING PROBLEM

As discussed in Section II, Deep Reinforcement Learning proved to be able to tackle challenging problems in several industrial applications with promising results. Therefore, in this paper we propose an algorithm based on Deep Q-Learning [31] to solve the multimodal online planning problem introduced in previous section. Algorithm 1 summarizes our Deep Q-learning method. We discuss the various components more in details in the following subsections.

### A. Multimodal Transportation Problem Environment

The DRL algorithm learns by performing a number of episodes \( E \). During each episode a set of containers is planned either on a train or on a truck. The environment
Algorithm 1 Deep Q-Learning for Online Multimodal Transportation Planning

1: Initialize Deep Q-Network $Q$
2: Initialize replay memory $D$
3: for episode = 1 to $E$ do
4: Generate new containers and trains
5: Set current state $s$ with random capacity for all trains
6: while there is an unassigned container $i \in I$ do
7: $A' \leftarrow \text{mask}(s)$ forbidden actions (Equation 7)
8: With probability $\epsilon$ select a random action $a \in A'$
9: Otherwise select $a = \text{argmax}_{a' \in A} Q(s, a')$
10: Create new state $s'$ from $s$ by updating train capacity used by $a$
11: Update new state $s'$ with next container
12: Calculate reward $r = R(s, a)$
13: Record experience $(s, a, r, s')$ in replay memory $D$
14: $s \leftarrow s'$
15: if every $M$ iterations then
16: Sample random minibatch of experience from replay memory $D$
17: for $(s, a, r, s')$ in minibatch do
18: $y \leftarrow \text{Bellman Equation over } (s, a, r, s'), Q$
19: Update Deep Q-Network $Q(s, a) = y$
20: end for
21: end if
22: end while

has the information on the trains and containers. It keeps a current state, and can be given actions to perform that will result in a reward and a new state (see Section III-B). To this end, the environment has two main functions:

- **Environment initialization.** At the beginning of each episode a new environment is generated by launching the data generator, to ensure that the starting point of each new episode is different from other episodes. The data generator creates: a set of trains with their temporal features and initial capacities, a set of containers, with their temporal features, and transportation costs for each vehicle option (Algorithm line 4).

- **Interaction with the agent.** For training the Deep Reinforcement learning model, we need to have interaction between the agent, model, and environment. In this interaction, we update the environment, calculate the next state and calculate reward of this action. In our problem, updating the environment means updating the capacity of trains based on the selected action (Algorithm line 10). Then, a new state is generated using the updated train capacities from the environment, and selecting the next container to plan (Algorithm line 11). The reward for the selected action (see Section IV-C) by our agent is the negative cost of the transportation associated with the selected action (Algorithm line 12).

We compare two different heuristics for selecting the next container to assign, (1) Earliest arrival first (or First In First Out - FIFO) and (2) Earliest due date first (EDF). Hereafter, we refer to the method implementing the FIFO and the EDF allocation heuristic as “DRL-FIFO” and “DRL-EDF”, respectively.

### B. Feature Engineering and Deep Q-Network Architecture

The algorithm learns through a Deep Q-Network, which learns the Q values for state/action combinations.

As explained in Section III-B, we use as input features of the network a vector of size $|T|+2$, which consists of a list of the number of spaces available on trains and both temporal features $e_l, t_l$ of container $i$. Accordingly, we have $|T|+2$ input nodes for the network. As output nodes, we use a separate output unit for each possible action. Hence, the size of our output layer is equal to the size of the vehicle options (A). The outputs of our Deep Q-Network correspond to the predicted Q-values of the individual action $a$ for the input state $s$. Fig. 2 shows the overall neural network architecture, that is a fully-connected neural network with $k$ hidden layers.

### C. Action Selection Methods and Masking Approach

In the transportation planning problem eligibility of actions changes dynamically (see Section III-B), with the result that the list of allowed actions can be different for each state $s$. However, the use of a dynamic set of actions increases significantly the complexity of the problem, up to the point where the computation is not feasible. To deal with this challenge, we determine a static actions list of all possible actions and then use a masking approach to determine which actions are enabled at each state $s$.

To select an action to perform in a state, we use a customized epsilon-greedy method with masking. More precisely, in a state we first determine the set of possible actions through masking (Algorithm line 7) as follows:

$$\text{mask}((\text{cap}_1, \ldots, \text{cap}_{|T|}, e, l)) = \{i \in T \mid d_i > e, ar_i \leq l, \text{cap}_i \geq 1\} \cup \{\text{Truck}\}$$

(7)

We then apply the epsilon-greedy method to the eligible actions $A'$ (Algorithm lines 8-9). In this method, the agent selects a random eligible action with a fixed probability, $0 \geq \epsilon \geq 1$, or the action that is optimal with respect to the learned Q-function otherwise [32].
D. Replay Memory and Minibatch

We use a replay memory [31]. In this method, we record the experiences of our agent into a replay memory \( D \) at each step \( (s,a,r,s') \) of each episode (Algorithm line [13]). Every \( M \) steps, we then update the Deep Q-Network with the new experiences. The main advantage of this method consists in decreasing the variance of the updates. Lines [15] to [19] show how we apply Q-learning updates, or minibatch updates, by first sampling experiences randomly from the replay memory, calculating the expected cumulative reward for each experience using the Bellman equation and then updating the Deep Q-Network for each experience with the calculated expected cumulative reward.

V. EXPERIMENTS AND RESULTS

In this section, we discuss the results of the experiments that we carried out to test the performance of our proposed methods. In Section V-A, we explain the dataset, the hyperparameter training setup, and the methods we tested in comparison to our approach. In Section V-B, we discuss the training and stability analysis. In Section V-C, we report the performance of our method, tested with both the discussed container selection heuristics, and the other competitor planning methods we tested, together with an analysis on the optimality gap between offline and online methods.

A. Experimental Settings

a) Dataset: For this experiment, we generated data with properties that are based on the long-haul transportation planning problem of a logistics company for a particular transportation corridor (i.e., the set of available transportation resources between two particular transshipment points). As discussed in Section IV, these data include the following features: the number of trains, the capacity and temporal properties of the trains, containers with their temporal features, and transportation costs. Time windows of this experiment are weekly. We assume that trucks are always available and the number of trucks is uncaptacitated. This is in line with the experience of the company that they can always find charter companies to transport containers by truck.

b) Training parameters: We did hyperparameter tuning on: the number of episodes (with options 1000, 2000, 3000, 4000), learning rate (0.01, 0.1), number of hidden layers (2, 4), discount factor (0.5, 0.99), number of nodes per hidden layer (100, 150, 200), and mini batch size (5, 10, 15). The algorithm worked best and learning converged using \( E = 4,000 \) episodes of 7 days. Note that the starting state of each episode is different from other episodes. In each episode 100 containers must be planned, i.e. 100 steps must be performed. The number of containers is chosen proportional to the train capacity over the week, in line with the properties of the planning problem at the logistics company. Each container has an earliest availability day that is uniformly distributed over the week. The due date is uniformly distributed over the days after the earliest availability day. There are 28 train schedules per week. For the capacity of trains in each train schedule we test 7 different settings, i.e.: 6 different settings in which each train schedule (1,1),(1,2),… has the same capacity 1 through to 6; and one setting in which each schedule has a random number of available slots that is uniformly distributed over 0 to 6 spaces. The goal of using these different capacity settings is to investigate the effect of the available capacity on the planners’ performance. We initialize a fully-connected feedforward neural network with backpropagation with 2 hidden layers of 100 nodes, ReLU activator, and Adam optimizer. We use a replay memory of size 10,000 and retrain the Deep Q-Network based on minibatches 5 times per epoch. The discount factor, used in the Bellman equation, is \( \gamma = 0.99 \). This means that we care more about the reward that is received in the future than the immediate reward. Remaining parameters are initialized according to PyTorch’s default parameters. The probability \( \varepsilon \) with which a random action is chosen starts at 0.95 and is decreased after each episode in steps of 0.1 until it reaches 0.05. The agent and the simulation model are executed on a machine with an Intel(R) Core(TM) i7 Processor CPU @ 2.80GHz and 16GB of RAM, no graphics module is used for training the neural network.

c) Planning Methods used for Comparison: We compare the performance of our method against the results obtained by two groups of methods: (1) ILP-based (re)optimization, and (2) Greedy heuristics. These methods are inspired by the existing literature [3] and discussions with the logistics company on how their online planner currently works. For the ILP-based planning, we run an ILP planner which returns a (sub) optimal, offline solution on the basis of the information known at a given moment in time. More precisely, we tested three different ILP-based planning methods. The first one, the ILP solver, is run once per week and has perfect knowledge on all the containers for that week, as defined in Section III-A. Consequently, this planner always produces the optimal solution. However, this solution is purely theoretical and only used for benchmarking, because the assumption that the precise arrivals of containers are all known at the start of the week is unrealistic. The 2-ILP planner is run twice per week, in both cases only with the information on the containers that have arrived up until and including the day of the planning. Finally, the 7-ILP planner is run daily, and also has information on containers that have arrived up until and including the day of the planning. While the ILP-solver computes the optimal solution for the offline planning problem, the 2-ILP and the 7-ILP only have limited information. These types of planners are commonly used in practice. The greedy heuristics, entitled First train and Cheapest train, assign each container separately to an eligible train that will take it to the destination on time and, if no such train is available, to a truck. The first greedy heuristic assigns a container to the first available train. The second one assigns a container to the cheapest available train. The comparison is based on the total cost of transportation over 200 weeks, i.e. 20,000 containers.
recognize learning allocation rules in DRL-EDF is faster than in DRL-FIFO.

C. Methods Comparison and Optimality Evaluation

In this subsection, we compare the performance of DRL-EDF and DRL-FIFO with the ILP-based optimization methods and the greedy heuristics we introduced before. The evaluation is performed based on the average of the total cost of transportation and utilization of capacity, that are computed respectively as the sum of all transportation costs of trains and trucks, and as the used train slots over each day. We tested these methods in different experiments with seven different capacity settings. Fig. 4 shows the distribution of the transportation costs and Fig. 5 shows the distribution of the capacity utilization of each method using histogram in the different capacity settings. The costs/utilization are computed as the average per week over 200 weeks. Fig. 4 and Fig. 5 show that in the most competitive scenario (i.e., with train capacity equal to 1) the tested methods mostly obtain similar results, even though 7-ILP and the greedy methods perform worse both in terms of total costs and train utilization. However, in all the remaining capacity settings, DRL-FIFO and DRL-EDF consistently outperform 2-ILP, 7-ILP and the greedy heuristics we introduced before. The differences are more evident with the increasing of the available capacity. Furthermore, the performance of DRL-EDF and DRL-FIFO in the random capacity setting.
TABLE III: Average differences with optimal solution over 200 weeks.

| Method         | Capacity utilization (%) | Total cost (%) |
|----------------|--------------------------|----------------|
| DRL-FIFO       | -1.62                    | +4.70          |
| DRL-EDF        | -0.72                    | +2.73          |
| 2-ILP          | -8.23                    | +23.21         |
| 7-ILP          | -21.26                   | +58.32         |
| First train    | -10.82                   | +34.08         |
| Cheapest train | -20.81                   | +56.95         |

This work investigated the application of Deep Reinforcement Learning in solving a challenging online planning problem in the multimodal transportation domain: the optimal assignment of containers to onward transportation, taking into account time, capacity constraints, and optimizing the total cost of transportation over all containers. We formulated the problem as a Markov Decision Process and, based on this formulation, we developed a DRL algorithm using two different allocation heuristics able to carry out online planning of single containers, with the goal of minimizing the overall transportation costs. The approach has been tested using data simulating a realistic scenario, designed on the basis of a real case study from a logistics company. The experimental results revealed that the proposed method is able to learn patterns of containers assignment in our scenario and the performance of the DRL-EDF is better than the one of DRL-FIFO. We have compared the performance of both DRL-EDF and DRL-FIFO against the results of two ILP based re-optimization methods and two greedy heuristics commonly used for online planning, as well as against the optimal ILP solution. The results show that the proposed DRL method outperformed the tested competitors in terms of total transportation costs and utilization of train capacity by 20.48% to 55.32% for the cost and by 7.51% to 20.54% for the capacity. Furthermore, it obtained results within 2.7% for the cost and 0.72% for the capacity of the optimal solution generated by an ILP solver in an offline setting. Overall, these results show

![Fig. 4: Average transportation cost of different methods over 200 weeks.](image)

![Fig. 5: Average capacity utilization of different methods over 200 weeks.](image)
how the use of AI-driven planners using Deep Reinforce-
ment Learning can significantly decrease costs associated to
container replanning for logistics companies, thus suggesting
that the use of these techniques can indeed bring significant
practical advantages in the logistic domain. Nevertheless, our
method presents some limitations that we plan to address in
future work. In particular, the current version of the method
has been designed and tested to support the allocation of
containers to a single vehicle, rather than to a combination of
vehicles. Furthermore, here we considered only two main
transportation modes, i.e., trains and trucks. In future work,
we plan to extend our model to incorporate these aspects,
thus increasing the generality of the methods. Also, we will
want to take locations as a planning factor into account.
Furthermore, we intend to integrate the uncertainty aspect
in the online planner algorithm. In particular, we intend to
investigate how to integrate knowledge about probabilities
of vehicles delay in the planning decision-making, to make
more effective and less costly allocation plans.

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