Nanoclusters first: a hierarchical phase transformation in a novel Mg alloy

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The Mg-Y-Zn ternary alloy system contains a series of novel structures known as long-period stacking ordered (LPSO) structures. The formation process and its key concept from a viewpoint of phase transition are not yet clear. The current study reveals that the phase transformation process is not a traditional spinodal decomposition or structural transformation but, rather a novel hierarchical phase transformation. In this transformation, clustering occurs first, and the spatial rearrangement of the clusters induce a secondary phase transformation that eventually lead to two-dimensional ordering of the clusters. The formation process was examined using in situ synchrotron radiation small-angle X-ray scattering (SAXS). Rapid quenching from liquid alloy into thin ribbons yielded strongly supersaturated amorphous samples. The samples were heated at a constant rate of 10 K/min. and the scattering patterns were acquired. The SAXS analysis indicated that small clusters grew to sizes of 0.2 nm after they crystallized. The clusters distributed randomly in space grew and eventually transformed into a microstructure with two well-defined cluster-cluster distances, one for the segregation periodicity of LPSO and the other for the in-plane ordering in segregated layer. This transformation into the LPSO structure concomitantly introduces the periodical stacking fault required for the 18R structures.

Metallic alloys undergo various types of phase transformations. These processes, including spinodal decomposition1, clustering2, order-disorder transition accompanying spinodal decomposition3, and displacive transformation4, have been the subjects of intense interest from a statistical thermodynamics viewpoint5,6 and from that of strategies for developing innovative materials. An understanding of these mechanisms can be extended to a much wider range of self-organized nanostructures, such as semiconducting nanodot heterostructures7, block copolymers8 and complex fluids9. We demonstrate that novel light weight Mg alloys with industrial interest10, Mg-Y-Zn ternary alloys, exhibit a novel spontaneously hierarchical phase transition, first clustering and second crystallization of clusters, i.e., ordering of the spatial arrangements of clusters, ultimately leading to order-disorder (OD) structures11,12.

An emerging group of Mg alloys, with a series of novel structures called synchronized long-period stacking ordered (LPSO) structures13,14, have attracted much attention for two reasons. One is interest in how and why such strange structure is stabilized, i.e., from phase transformation viewpoints. The other reason is interest in their mechanical properties, i.e., higher strength for practical applications ranging from mobile computers to aircrafts, and basic questions about the kink deformation mechanism15,16.

The LPSO phase was first observed in MgZnY alloys as a periodic concentration modulation of Zn and Y along the c axis13,14 in an hcp Mg matrix, and then a more refined structure was determined by electron microscopic works focusing on determining equilibrium (stable) structures of LPSO phases17,18.
Figure 1. Schematic illustration of a fully ordered 18R structure reported by Yokobayashi et al. for MgGdAl alloys. L1_2 clusters form a $2\sqrt{3} \times 2\sqrt{3}$ order structure at the stacking faults (SFs). For the MgYZn LPSSO structure, Gd is replaced by Y and Al is replaced by Zn. Y atoms occupy 8 corner positions and Zn atoms occupy the face-centre positions for a Y_{8}Zn_{6} cluster.

A reported structure is schematically illustrated in Fig. 1. The segregation layers consist of a two-dimensionally ordered arrangement of L1_2-type $Y_{8}Zn_{6}$ or Gd_{6}Al_{6} molecular-like clusters with $2\sqrt{3} \times 2\sqrt{3}$ superstructures, whose stacking in the perpendicular direction is described by crystallographic operations. The structure appears similar to that of intermetallic compounds with well-defined atomic positions and occupancies. However, upon examining the temporal structural change using synchrotron radiation small-angle scattering (SR-SAXS), we observed that the distance between the ordered clusters changed continuously with time within the segregation plane. The in-plane structure shown in Fig. 1 appears to undergo a two-dimensional order-disorder transition of clusters. Such superstructures by clusters in the segregation layer might be examined in terms of two-dimensional phase transformations of particles similar to colloidal crystals. The confinement of the L1_2-ordered clusters occurs in two-dimension, as if the clusters, a partial structure of a complex order structure, behave as an independent structure unit. It should be noted that the system is three-dimensional, and the formation and growth of such clusters are driven by the same phase transformation process. Knowing this, we need to return to the question of how we can understand the stability and formation mechanism of the LPSSO structures in three dimension in relation to the two-dimensional order-disorder behaviour.

In many metallic alloys, a phase transition is observed upon quenching materials from a high temperature (higher symmetry) phase into a supersaturated state. For example, by quenching Al alloys, clusters of a minority phase called Guinier-Preston (GP) zones develop, whose characteristic lengths, such as their average sizes, grow with a temporal power law. Comparison of the growth power law with the prediction from cluster dynamics theories or simulations provides an image of the transformation, such as the centre of gravity of the nanoclusters moving (diffusion of clusters), and their coagulation during the early stage of precipitation. When the volume fraction of a minority phase is large, spinodal decomposition or spinodal ordering is expected. For the present Mg_{85}Y_{9}Zn_{6} alloys, thermodynamical analysis suggested possibility of spinodal decomposition as the major driving force of LPSSO formation. However, the periodic stacking faults in the LPSSO structures, as shown in Fig. 1 starts another discussion from a structural phase transformations viewpoint, i.e., stacking-fault driven transformation. However, neither of the mechanisms appears to be compatible with the two-dimensional ordering kinetics of the present alloys described above.

Results and Discussions

To examine the initial stage of the formation process, small-angle X-ray scattering (SAXS) patterns were measured in situ while heating rapidly quenched Mg_{85}Y_{9}Zn_{6} ribbons. The sample ribbons were initially glassy and uniform at the macroscopic length scale. A single-phase 18R LPSSO microstructure is reported for the composition after long-time annealing.

Figure 2 shows the change in the SAXS profile during heating. The round shoulders of the scattering intensities in the figure indicate that many small clusters stably exist even at low temperatures, and grow as the temperature increases. Another important point is that the scattering pattern changes the shape from a single diffuse peak to a double sharp peak profile at higher temperatures. With a cluster model, a scattering profile is approximated by the cluster component (form factor, $F(q)$) and the spatial arrangements of the clusters (structure factor, $S(q)$ ), as:

$$I(q) = F^2(q)S(q).$$

(1)
where $q$ is the magnitude of scattering vector. The average radius obtained from the form factor is shown in Fig. 3. It is approximately 0.14 nm before crystallization, and a rapid increase to a radius of approximately 0.2 nm was observed when crystallization occurred. The cluster size increased with temperatures, and the growth slowed down at the radius of 0.34 nm at 570 K. The gyration radius of the L1₂ cluster obtained from a first-principles calculation of the MgYZn LPSO structure is 0.34 $\pm$ 0.01 nm, which implies that the early stage of the phase transition should be described by a cluster image, not by classical spinodal decomposition.

Figure 4 shows the structure factors for several temperatures and corresponding schematic illustrations of the nanostructures in the sample. At lower temperatures, the structure factor is characterized by a single diffuse peak, suggesting that the clusters are distributed isotropically in the amorphous or crystal matrix. At higher temperatures above 553 K, the peak of the structure factor begins to separate into two peaks, one for 18R concentration modulation and the other for in-plane ordering. The clear peaks at approximately 4 nm$^{-1}$ and 6 nm$^{-1}$ are the fingerprint of the 18R LPSO structure.

Figure 2. In-situ small-angle scattering during heating (a) below and (b) above the crystallization temperature, $T_x$. The shoulder denoted as cluster in (a) represents scattering by small clusters distributed isotropically in space. At higher temperature (b), a diffuse peak in (a) decomposed into two peaks, one for 18R concentration modulation and the other for in-plane ordering. The clear peaks at approximately 4 nm$^{-1}$ and 6 nm$^{-1}$ are the fingerprint of the 18R LPSO structure.
similar to clusters in Al-Zn. The difference between the two alloys is that the clusters in LPSO stopped growing at the size of \( Y_6Zn_6 \) and formed cluster crystals like colloid crystals with two characteristic distances, an interlayer and intralayer distances. After such separation started above 530 K, where the clusters align in a plane, cooperative shear transformed the hcp-based clusters with \( DO_{19} \) into fcc-based clusters with \( L1_2 \). Using first-principles calculations, the energy gain associated with the transformation from \( Y_6Zn_6 + Y_2 \) clusters on an hcp lattice into a \( Y_8Zn_6 \) \( L1_2 \) cluster was estimated to be at least 1.86 eV per \( L1_2 \) cluster. Assuming a \( 2\sqrt{3} \times 2\sqrt{3} \) and even coarser superstructure, this energy gain sufficiently overcomes the energy loss caused by stacking-fault formation in the surrounding Mg matrix. Then the clusters are pinned by the stacking fault and two-dimensional self-organization\(^{20,21}\) begins. An interesting

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**Figure 3.** Cluster size determined from \textit{in situ} SAXS. The size of the clusters remained at 0.14 nm in the glass structure and then rapidly increased to 0.2 nm upon crystallization \((T_x)\). The growth slowed down when the size reached that of the \( L1_2 \) cluster in stable 18R structure.

**Figure 4.** Structure factors and corresponding schematic illustrations of the microstructure during heating. After crystallization, the structure factor results in a well-defined single diffuse peak, suggesting isotropic distribution of the clusters. The average distance between the clusters splits into two groups of distances, one leading to the interlayer distance and the other to the intralayer (in-plane) distance.
point here is that the clusters of Y and Zn are stable enough to exist even in amorphous state, but never grow larger than the size of approximately one unit cell, resulting in a stable size of molecular-like \( Y_2Zn_6 \) clusters in the crystalline state. Sharp diffraction peaks from concentration modulation for the periodicity of 18R up to the second order peak at 8 nm\(^{-1}\) and in-plane diffraction peak agreed with those for cast samples annealed for long time, whose structure has been well examined by TEM\(^{10,13,18}\) are the signature of formation of 18R structure.

We may refer to two systems that exhibit similar nanostructures: perforated structures in block copolymer systems\(^{31}\) and confined colloidal crystal systems\(^{32}\). A perforated nanostructure in a block copolymer forms two-dimensional ordered layers self-organized in three-dimensional materials, however, it is different from the present case in that further two-dimensional ordering transition is not observed. Confined colloidal crystals do exhibit two-dimensional phase transition, however, the origin of confinement is external. In contrast, the clusters in the present alloy grows and voluntarily form two-dimensional cluster layers, and then the two-dimensional order of the cluster proceeds, finally leading to interlayer (OD) ordering. An interesting point here is that these hierarchical transitions are driven by the single free energy curve of the LPSO alloy, with a different magnitude of interaction depending on the hierarchy. In short, a strong phase separation tendency\(^{29}\), repulsive, but much weaker interaction between the clusters\(^{22}\), and even weaker energy gain with OD structures are the key to understand the present case. Further systematic investigation of the related alloy will provide us with a perspective on alloy design and help determine how the magnitude of interaction be implemented to design building blocks in artificial nanostructures such as functional colloidal crystals.

In summary, we demonstrated that the key to understand the formation of LPSO in the present alloy is neither typical spinodal decomposition\(^{11}\) nor structural transformation\(^{4}\). The kinetics indicated a hierarchical phase transformation sequence of clustering first, followed by cluster motion for long-period structures with the introduction of stacking faults. Finally two-dimensional nanoscopic ordering in segregation layers was observed.

Methods

Small-angle X-ray scattering (SAXS) measurements were applied to examine the nanoscopic heterogeneity in the sample. Mg\(_{85}\)Y\(_9\)Zn\(_6\) alloy, the composition for single phase 18R LPSO, was rapidly quenched (RQ) from a liquid into amorphous ribbons. The ribbons were heated at a speed of 10K/min. from room temperature to melting in a furnace with carbon insulation and evacuated using a turbo molecular pump. SAXS profiles were acquired every 15 to 20 seconds in situ during heating. Calorimetric measurements were made separately to detect the transformation temperatures. XAFS measurements were preformed for as-quenched and annealed ribbons at the K absorption edge of Zn and Y, and were compared with the results for cast ingots annealed at 673 K for a month. The ribbons were isothermally annealed for 5 minutes in sealed Pyrex\textsuperscript{®} tube at the temperatures between 423 K and 582 K. The energetics and equilibrium structure of Mg-Y-Zn systems containing a solute cluster were obtained from first-principles density functional theory (DFT) calculations using the VASP code\(^{32}\).

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**Author Contributions**

H.O. conducted and analysed the small-angle scattering and wrote the draft. M.Y. and Y.K. designed, prepared the sample and preformed the thermal analysis. M.T. and H.O. worked on the XAFS measurements and analysis. H.K. performed the model cluster structures calculations using a first-principles approach.

**Additional Information**

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