Illuminating the dark ages: cosmic backgrounds from accretion onto primordial black hole dark matter

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Abstract. The recent interpretation of cold dark matter as the sum of contributions of different mass Primordial Black Hole (PBH) families [1] could explain a number of so far unsolved astrophysical mysteries. Here I assume a realistic $10^{-8} - 10^{10} \, M_\odot$ PBH mass distribution providing the bulk of the dark matter, consistent with all observational constraints. I estimate the contribution of baryon accretion onto this PBH population to various cosmic background radiations, concentrating first on the cross-correlation signal between the Cosmic X-ray and the Cosmic infrared background fluctuations discovered in deep Chandra and Spitzer surveys. I assume Bondi capture and advection dominated disk accretion with reasonable parameters like baryon density and effective relative velocity between baryons and PBH, as well as appropriate accretion and radiation efficiencies, and integrate these over the PBH mass spectrum and cosmic time. The prediction of the PBH contribution to the X-ray background is indeed consistent with the residual X-ray background signal and the X-ray/infrared fluctuations. The predicted flux peaks at redshifts $z=17-30$, consistent with other constraints requiring the signal to come from such high redshifts. The PBH contribution to the $2-5 \, \mu m$ cosmic infrared background fluctuations is only about 1%, so that these likely come from star formation processes in regions associated with the PBH.

I discuss a number of other phenomena, which could be significantly affected by the PBH accretion. Magnetic fields are an essential ingredient in the Bondi capture process, and I argue that the PBH can play an important role in amplifying magnetic seed fields in the early universe and maintaining them until the galactic dynamo processes set in. Next I study the contribution of the assumed PBH population to the re-ionization history of the universe and find that they do not conflict with the stringent ionization limits set by the most recent Planck measurements. X-ray heating from the PBH population can provide a contribution to the entropy floor observed in groups of galaxies. The tantalizing redshifted 21-cm absorption line feature observed by EDGES could well be connected to the radio emission contributed by PBH to the cosmic background radiation. Finally, the number of intermediate-mass black holes and the diffuse X-ray emission in the Galactic Center region are not violated by the assumed PBH dark matter, on the contrary, some of the discrete sources resolved in the deepest Chandra observations of the Galactic Ridge could indeed be accreting PBH.

Keywords: primordial black holes, primordial magnetic fields, recombination, X-rays

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1 Introduction

Recent years saw a revival of the idea originally put forward by S. Hawking [2], that Primordial Black Holes (PBH) could make up the so far elusive Dark Matter. LIGOs first detection of gravitational waves from merging binary black holes of approximately equal masses in the range 10–30 M⊙ [3, 4] led to the suggestion that these could be a signature of dark matter stellar mass PBH [5–7] in a mass window not yet excluded by other astrophysical constraints. A recent review about the rich literature constraining the possible contributions of PBH to the dark matter is e.g. given in [8].

In a recently published theoretical prediction [1, 9] PBH are created in the QCD phase transitions (around 100 MeV) of different particle families freezing out of the primordial Quark-gluon plasma within the first two seconds after the inflationary phase. When W⁺/−, Z bosons, baryons, pions are created, and e⁺e⁻ pairs annihilate, they leave an imprint in form of a significant reduction of the sound speed at the corresponding phase transitions, and allow regions of high curvature to collapse and form PBH (see also [10]). The typical mass scale of these PBH is defined by the size of the horizon at the time of the corresponding phase transition. In this model four distinct populations of PBH in a wide mass range are formed: planetary mass black holes at the W⁺/−, Z transition, PBH of around the Chandrasekhar mass when the baryons (protons and neutrons) are formed from 3 quarks, PBH of masses of order 30 M⊙ (these correspond to the LIGO black holes), when pions are formed from two quarks, and finally supermassive black holes (SMBH) at the e⁺e⁻ annihilation (see also [11]).

Another remarkable aspect of this theory is, that the gravitational energy released at the PBH collapse locally reheats regions (hot spots) around the black holes to the electroweak transition scale (around 100 GeV), where chiral sphaleron selection effects can introduce the matter/antimatter asymmetry. The PBH in this picture would therefore also be responsible
for the baryogenesis and fix the ratio of dark matter to baryons. Clustering of the PBH in a very wide mass distribution could alleviate some of the more stringent observational constraints on the allowed contribution of PBH to the dark matter [7, 12]. The interpretation of cold dark matter as the sum of contributions of different mass PBH families could explain a number of so far unsolved mysteries, like e.g. the massive seed black holes required to create the supermassive black holes in the earliest QSOs [13], the ubiquitous massive LIGO/VIRGO massive binary black holes (e.g. [6]), or even the putative "Planet X" PBH in our own Solar System [14].

The most abundant family of PBH should be around the Chandrasekhar mass ($1.4 \, M_{\odot}$). This prediction may already have been vindicated by the recent OGLE/GAIA discovery of a sizeable population of putative black holes in the mass range $1-10 \, M_{\odot}$ [15]. The microlensing survey OGLE has detected $\sim 60$ long-duration microlensing events. About 20 of these have GAIA DR2 parallax distances of a few kpc, which break the microlensing mass-distance degeneracy and allow the determination of masses in the few solar mass range, implying that these objects are most likely black holes, since stars at those distances would be directly visible by OGLE.

Important fingerprints of a population of PBH may be hidden in the Cosmic infrared and X-ray background radiation (see [16] for a comprehensive review). Indeed, [6] argues, that the near-infrared Cosmic background (CIB) anisotropies detected in deep Spitzer [17–20] and Akari [21] images, which cannot be accounted for by known galaxy populations [22], could be connected to PBH. Similar fluctuations were discovered in the Cosmic X-ray background (CXB) observed in a deep Chandra survey, which are correlated with the CIB anisotropies in the same field [23]. Later studies of wider/deeper fields covered by both Chandra and Spitzer [24–26] have substantially improved the detection significance of the observed signal. The X-ray fluctuations contribute about 20% to the CIB signal, indicating that black hole accretion should be responsible for such highly efficient X-ray emission. Similar studies of deep fields observed with the Hubble Space Telescope in the optical range do not show such a cross-correlation signal down to $m_{AB} \sim 28$ [see 16]. The angular scale of the fluctuation power spectra of the CIB and CXB reach values $>1000''$, much larger than expected for the known galaxy populations [27]. All of these findings can be understood, if the fluctuation signal comes from a high-redshift ($z \gtrsim 12$) population of black holes. The spectral shape of the CXB fluctuations determined from a combination of the deepest/widest fields [26] can be fit either with a very high redshift population of obscured black holes, or with completely unobscured black hole accretion. Original models [28] invoked highly obscured Direct Collapse Black Holes formed in metal-free halos at $z>12$ to explain the observed CIB and CXB signal. However, accreting massive black holes have recently been firmly ruled out as the source of these fluctuations [29], because they would require an unfeasible amount of black hole accretion at $z>6$, locking up a larger amount of mass in massive black holes at high redshift, than the known black hole mass function at $z=0$. These authors also ruled out local diffuse emission as the source of the X-ray fluctuations. The CXB has been largely resolved into discrete sources in deep X-ray images, either directly (see [30, 31]), or by crosscorrelating with the deepest Hubble galaxy catalogues [32, 33]. However, [32] show that some marginally significant diffuse CXB still remains after accounting for all discrete contributions. This is consistent with the independent determination of [34]. The residual unresolved flux is about 3 times larger than the X-ray flux associated with the above CXB/CIB fluctuations.

Given the difficulties in explaining the CIB/CXB correlation with known classes of sources, and motivated by the notion that the dark matter could be dominated by an extended
mass distribution of PBH, I constructed a toy model to explore the potential contribution to the cosmic backgrounds by the accretion of baryons throughout cosmic history onto such a population of early black holes. Assuming a combination of Bondi-Hoyle-Lyttleton quasi-spherical capture at large distances from the PBH, and advection-dominated disk accretion flows (ADAF) in the vicinity of the central object, I can explain the observed residual CXB flux and the CXB/CIB cross-correlation with minimal tuning of the input parameters, and find a maximum contribution to the extragalactic background light in the redshift range $15 < z < 30$. I further estimate that this accretion onto PBH can produce enough flux to significantly contribute to the pre-ionization of the intergalactic medium with UV photons by a redshift $z \gtrsim 15$ and to the pre-heating of the baryons with X-ray photons, observed as an "entropy floor" in the X-ray emission of galaxy groups.

In section 2 the assumed PBH mass distribution is introduced and contrasted with recent observational limits on the PBH contribution to the dark matter. The basic ingredients of the toy model for the accretion onto PBH are presented in section 3. The assumed radiation mechanism and efficiency is discussed in section 4. The contribution of the PBH emission to the different bands is compared with the observational constraints in section 5. Other potential diagnostics of this putative dark matter black hole population are discussed in section 6, and conclusions are presented in section 7. Throughout this work a $\Lambda$CDM cosmology with $\Omega_M=0.315$, $\Omega_\Lambda=0.685$, and $H_0=67.4\,\text{km}\,\text{s}^{-1}\,\text{Mpc}^{-1}$ [35] is used. These parameters define the baryon density $\Omega_{\text{bar}}=0.049$, the dark matter density $\Omega_{DM}=0.264$, and the critical mass density of the universe $\rho_{\text{crit}}=1.26\times10^{20} M_\odot\,\text{Gpc}^{-3}$. All logarithms in this paper are taken to the base 10.

2 The assumed PBH mass distribution

The theoretical predictions in [1, 9, 11, 36] yield a broad distribution of PBH masses with a number of peaks corresponding to the particle families freezing out from the Big Bang. Depending on the spectral index $n_s$ of the primordial curvature fluctuation power spectrum, the PBH mass distribution has a different overall slope. [36] find consistency of these predictions with a number of recent observational limits on the PBH contribution to the dark matter, but there is a tension of their models with the Cosmic Microwave Background (CMB) constraints from accretion at large PBH masses [37, 38]. Recent limits from gravitational lensing of type Ia supernovae on a maximum contribution of stellar-mass compact objects to the dark matter of around 35% [39], and from the LIGO OI gravitational wave merger rate of black holes in the mass range 10–300 $M_\odot$ [40] are also in tension with these models. An additional important constraint comes from a comparison of the predicted PBH fraction with the measured local mass function of supermassive black holes (SMBH) in the centers of nearby galaxies. Integrating the local SMBH mass function of [41] (see figure 1) in the range $10^6$–$10^{10} M_\odot$ yields a local SMBH mass density of $\rho_{SMBH}=6.3\times10^5 M_\odot\,\text{Mpc}^{-3}$, corresponding to a dark matter fraction of $f_{SMBH}=1.89\times10^{-5}$, which is about a factor of 10–100 lower than the $f_{PBH}$ predictions in [1, 36].

For these reasons, García-Bellido et al. (2020 in prep.) are revising their model parameters in order to predict a steeper PBH mass function at large $M_{PBH}$ and shared one of their new models, shown as red curve in figure 1. Here a value of $n_s=0.987$ is assumed for the spectral index of the primordial fluctuation power spectrum, as well as a running curvature of $dn_s=-0.0006$. The integral of this PBH distribution over the whole mass range yields $f_{PBH}=1$. On the other hand, the distribution yields only $\sim40\%$ of the dark matter in the
Figure 1. The PBH mass spectrum (thick red line) assumed for this work (García-Bellido, 2020, priv. comm.), compared to a number of observational constraints. Microlensing limits from SNe [39], EROS [42], and the Subaru M31 survey [43] are shown as solid, dashed and dotted green lines, respectively. LIGO limits from gravitational merger event rates are shown as blue solid line for subsolar masses [44], and as blue dashed line for 10-300 $M_\odot$ [40]. The CMB accretion limits from [37] are shown as orange dashed line. Multiwavelength limits from the Galactic Center [45] are shown in magenta for X-ray (solid) and radio (dashed) observations. Finally, the local SMBH mass function [41] is shown as black line at $10^6-10^7 M_\odot$.

peak mass range [0.1,10] $M_\odot$, and is thus fully consistent with the microlensing constraints in figure 1. In the mass range of the LIGO black hole binaries it predicts just the right amount of dark matter to explain the gravitational wave merger rates, and in the SMBH range it is consistent with the local black hole mass function (taking into account the accretion onto supermassive PBH over cosmic time producing the bulk of the X-ray background [46]). Apart from small sections, the new PBH mass function is thus fully consistent with the most recent observational constraints.

3 Baryon accretion onto the PBH

In the following I use the PBH mass spectrum presented in section 2 to calculate the accretion of baryons onto PBH over cosmic time, and to predict the electromagnetic emission from this process. As we will see, for most of the cosmic history these black holes move at supersonic speeds among the baryons and will therefore undergo Bondi-Hoyle-Lyttleton quasi-spherical capture [47–50]. In the Bondi-Hoyle picture of a black hole moving supersonically through a homogeneous gas, the capture happens in the wake of the moving object. Behind the object, material moves in from a wide cone, and needs to lose angular momentum before it can fall towards the black hole. The gas is in principle collisionless, so that only the magnetic field trapped in the plasma allows particles to lose angular momentum and start to behave like a fluid. This gas forms the accretion flow, in which it is adiabatically heated. The accreting
gas is ionized and embedded in the magnetic field. Any plasma drawn in by the gravitational field will carry along the magnetic field. Shvartsman [51] argues that in the black hole tail, where the matter flow stops, the gravitational and magnetic energy densities become nearly equal. This equipartition is preserved in the infalling flow and thus the magnetic field grows towards the black hole. Like the heat has to be ultimately radiated away, the magnetic field needs a way to dissipate energy on its way inward. [52] discuss that the most likely dissipation mechanism for the magnetic field is reconnection of field lines in narrow current sheets, similar to the processes we observe in solar flares and active galactic nuclei. Magnetic reconnection causes the acceleration and non-thermal heating of a small fraction of the infalling electrons. In parallel, decoupled magnetic field lines can carry some of the amplified magnetic field outward and eject plasma [52].

An important question is, whether the accretion flow is spherically symmetric close to the black hole, or whether an accretion disk is formed. Originally most researchers assumed spherical accretion for PBH [e.g. 38, 53, 54]. However, [37] argues, that the accreted angular momentum is large enough, that an accretion disk is formed, at least close to the black hole. According to these authors, the granularity of the PBH distribution and the formation of PBH binaries at the scale of the Bondi radius will imprint density and velocity gradients into the relative distribution of baryons and PBH, such that ultimately an accretion disk and an advection-dominated accretion flow (ADAF) will form [55]. The formation of an ADAF disk significantly reduces the accretion rate and the radiative efficiency [56], compared to spherical accretion. But to first order the Bondi-Hoyle-Lyttleton mechanism can be used to estimate the accretion rate $\dot{M}$ onto the PBH [8, 37].

Bondi [49] discusses two different approximations to the spherical gas accretion problem, (i) the velocity-limited case, where the motion of the accreting object through the gas is dominant and an accretion column is formed in the wake of the moving object, and (ii) the temperature-limited case, where the sound speed of the gas is dominant and a spherical accretion flow forms. In the velocity-limited case (i) the mass accretion rate is given as

$$\dot{M} = 2.5\pi \rho (GM)^2 v_{\text{rel}}^{-3},$$

(3.1)

where $\rho$ is the gas density, $M$ is the PBH mass, and $v_{\text{rel}}$ is the relative velocity between object and gas. In the temperature-limited case (ii) with negligible relative velocity, the thermal velocity of the gas particles is dominant and the corresponding accretion rate is given by

$$\dot{M} = 2.5\pi \rho (GM)^2 c_s^{-3},$$

(3.2)

where $c_s$ is the sound speed. For intermediate cases, [49] introduces an effective velocity

$$v_{\text{eff}} = \sqrt{v_{\text{rel}}^2 + c_s^2}$$

(3.3)

and the corresponding mass accretion rates becomes

$$\dot{M} = 2\lambda\pi \rho (GM)^2 v_{\text{eff}}^{-3},$$

(3.4)

where the so called accretion eigenvalue $\lambda$ is is a fudge factor of order unity, dependent on non-gravitational aspects of the problem, like e.g. the gas equation of state or outflows from feedback effects. Different authors have discussed this parameter for the particular application of gas accretion onto PBH in the early universe. [53] find values of $1.12 > \lambda > 10^{-3}$, depending e.g. on the PBH mass. For masses of order 1 $M_\odot$ they find $\lambda = 1.12$. 
discriminate between isothermal and adiabatic gas with accretion eigenvalues of $\lambda=1.12$, and 0.12, respectively. In this paper I assume an eigenvalue $\lambda=0.05$. The motivation for this choice is discussed in section 4, while section 5 and 6 show that this choice fits the observational constraints quite well.

Let us first look at the thermal history and thus the sound speed of the gas over cosmic time. A nice summary is given in figure 15 of [57]. Despite having decoupled from the CMB at $z \approx 1089$, the gas temperature continues to follow the temperature evolution $T \propto (1+z)$ of the background photons due to Compton scattering off residual ionized electrons from the recombination era. Below redshifts $z \approx 200$ the residual ionization in the gas is low enough, that it decouples from the background radiation and cools adiabatically following the relation $T \propto (1+z)^2$. When the first objects form and reionization starts around $z \lesssim 20$, the gas is heated up to temperatures $\sim 10^4$ K. The details of re-ionization are still uncertain and will be discussed below. I have deliberately chosen a redshift of $z \approx 20$ for re-ionization to become dominant, with full ionization occurring around $z \approx 7$. Finally, at $z < 3$, when the bulk of the cosmic baryons are falling into increasingly larger dark matter halos and become virialized, they are further heated up to form the warm/hot intergalactic medium at temperatures $10^5 - 7$ K [58]. Using figure 2b in this paper I estimate average temperatures for the IGM of $5\times10^4$, $1.5\times10^5$, and $8\times10^5$ K at $z=2, 1, 0$, respectively. The baryon temperature as a function of redshift assumed in this work is shown in figure 2 (left). The sound speed of the gas is given by

$$c_s = \sqrt{\frac{\gamma kT}{\mu m_H}},$$

where $\gamma=5/3$ for an ideal monoatomic gas, $\mu=1.22$ is the mean molecular weight including a helium mass fraction of 0.24, $m_H$ is the mass of the hydrogen atom, and $T$ is the temperature of the baryons as a function of cosmic history discussed above [59]. The sound speed as a function of redshift is the dotted curve shown in figure 2 (right).

I now discuss the relative velocity $v_{rel}$ between the dark matter PBH and the baryons throughout cosmic history. In the radiation-dominated phase of the universe at $z > 1089$, the
dark matter is already hierarchically clustering under the influence of its own gravity. The sound speed of the photon-baryon fluid is very high, of order one third of the velocity of light, and thus the normal matter undergoes baryonic acoustic oscillations [60, 61]. This leads to a spatial separation between baryons and dark matter and thus to a Gaussian distribution of relative velocities with an average around \( \langle v_{\text{rel}} \rangle \approx 30 \text{ km/s} \) (see [59, 62]). At \( z \approx 10^8 \), when electrons and protons combine and the universe becomes transparent, the sound speed of the gas dramatically drops to \( \sim 6 \text{ km/s} \). The dark matter PBH kinematically decouple from the baryons and their relative velocities become highly supersonic. In the linear growth phase of the universe, at scales larger than the gas Jeans-length, the dark matter and the baryons fall in the same gravitational potentials of the cosmic web and thus their relative velocity decreases with the cosmic expansion:

\[
\langle v_{\text{rel}} \rangle_{\text{linear}} \approx 30 \frac{1 + z}{1000} \text{ km s}^{-1}.
\] (3.6)

This relation is shown as the right branch of the dashed line in figure 2 (right), above redshifts \( z \gtrsim 20 \). From this figure it becomes apparent, that between recombination and re-ionization the PBH move with highly supersonic, but decreasing velocities through the gas, due to the decaying sound waves. As we will see below, in this branch of the velocity curve the contribution of PBH to the cosmic backgrounds has a maximum. At lower redshifts, at scales smaller than the gas Jeans-length, the hierarchical clustering becomes non-linear and baryons falling into growing dark matter halos are virialized. As a consequence, the velocity dispersion between dark matter and gas increases again towards lower redshifts, scaling as \( M_{\text{Halo}}^{1/3} \), where \( M_{\text{Halo}} \) is the mass of the dark matter halo becoming non-linear. I used two different methods to estimate the average virial velocity for redshifts \( z \leq 20 \). First, the Millenium Simulation run described in [63] gives the mass function of dark matter halos with halo masses \( M_{\text{Halo}} > 10^{10} M_\odot \) for five different redshifts between \( z = 10 \) and \( z = 0 \). I extrapolated these simulated mass functions to lower masses \( M_{\text{Halo}} > 10^3 M_\odot \) using the empirical universal halo mass function shape found through simulations by [64]. For every mass bin I determined the virial velocity according to the calibration of the velocity dispersion as a function of halo mass described in [65], and then calculated the average for each epoch. These virial velocities are shown as crosses in figure 2 (right). The extrapolation to halo masses as small as \( M_{\text{Halo}} > 10^3 M_\odot \) is rather uncertain, both for the mass function and the velocity dispersion, because the cosmological simulations do not have a fine enough mass resolution at this scale. Also, the velocity dispersion relevant for Bondi capture onto PBH is determined by the smallest mass scales becoming non-linear at any redshift. A second possibility to calculate the relative velocities in the non-linear phase is therefore to determine the velocity dispersion directly from the dark matter power spectrum and integrate this over the smallest non-linear scales. This calculation has been performed by M. Bartelmann (2020, priv. comm.), adopting the normalization of the primordial power spectrum of \( \sigma_8 = 0.8 \). The relative velocity in the non-linear regime can be approximated by

\[
\langle v_{\text{rel}} \rangle_{\text{nonlinear}} \approx 620 (1 + z)^{-2.3} \text{ km s}^{-1},
\] (3.7)

and is shown as the left branch \( (z \lesssim 20) \) of the dashed line in figure 2 (right). At \( z = 2 \) the cluster velocity dispersion agrees with this estimate, but it systematically overestimates the small-scale velocity dispersion at larger redshifts.

Since we are interested in the total contribution of PBH to the electromagnetic radiation of the universe, we have to average over the whole Gaussian distribution of relative velocities.
The Bondi accretion rate is proportional to $v_{\text{rel}}^{-3}$ (see above), and therefore smaller velocities dominate. For this particular case [38] propose to replace the quadratic average of relative velocity and sound speed in Bondi’s formula (3.3) above with their harmonic mean:

$$v_{\text{eff}} = \sqrt{\langle v_{\text{rel}} \rangle c_s}. \quad (3.8)$$

This is the assumption I adopt here, and the resulting effective velocity $v_{\text{eff}}$ is shown as solid red curve in figure 2 (right). With equation (3.8) the accretion rate becomes

$$\dot{M} = 2\pi\rho (GM)^2 (\langle v_{\text{rel}} \rangle c_s)^{-3/2} \quad (3.9)$$

It is interesting to note that in the range $200 < z < 20$ both relative velocity and sound speed decrease linearly with $(1+z)$. Therefore the mass accretion rate is expected to be constant in this era. It is important to understand that the redshift, at which both the sound speed and the relative velocity of the gas turn around due to re-ionization and virialization, respectively, and rapidly increase towards lower redshift, is crucial for our analysis. The redshift, where the minimum velocity occurs, ultimately determines the maximum flux contribution of PBH accretion to the cosmic backgrounds.

The calculation of the Bondi accretion rate in equation (3.9) requires the density $\rho$ as a function of redshift. With $\Omega_{\text{bar}}=0.049$ and $\rho=\text{n} \cdot m_H$, where $n$ is the number density of particles, I find

$$n = 250 \left( \frac{1+z}{1000} \right)^3 \text{cm}^{-3}. \quad (3.10)$$

I define $\dot{m}$ as the normalized mass accretion rate $\dot{m} = \dot{M}/\dot{M}_{\text{Edd}}$, with the Eddington accretion rate $\dot{M}_{\text{Edd}}=1.44 \times 10^{17} M_\odot \text{ g s}^{-1}$. Then I can rewrite equation (3.9) into normalized quantities

$$\dot{m} = \lambda \cdot 0.321 \left( \frac{1+z}{1000} \right)^3 \left( \frac{M}{M_\odot} \right) \left( \frac{v_{\text{eff}}}{1 \text{ km s}^{-1}} \right)^{-3} \quad (3.11)$$

With a very broad PBH mass spectrum, including intermediate-mass and supermassive black holes ($M_{PBH} > 1000 M_\odot$), it is important to include the effective viscosity due to the Hubble expansion in the early universe [53]. The Bondi radius determines the amount of mass captured by the PBH:

$$r_B = \frac{GM}{v_{\text{eff}}^2} \approx 1.34 \cdot 10^{16} \left( \frac{M}{M_\odot} \right) \left( \frac{v_{\text{eff}}}{1 \text{ km s}^{-1}} \right)^{-2} \text{ cm}. \quad (3.12)$$

This is shown for two different PBH masses in figure 8 (left). The characteristic time scale for accretion is the Bondi crossing time $t_{\text{cr}} = r_B/v_{\text{eff}}$, which can be compared to the Hubble time $t_H$ at the corresponding redshift. If $t_{\text{cr}} < t_H$ there will be stationary accretion, while for Bondi crossing times larger than the Hubble time the accretion is suppressed. For every redshift we can calculate a critical PBH mass $M_{\text{cr}}$, below which the steady-state Bondi assumption can be applied. For redshifts $z=1000, 200, 20$ this critical mass corresponds to $\log(M_{\text{cr}}/M_\odot) = 5.3, 4.8, 3.4$, respectively. At redshifts below $z=20$ $M_{\text{cr}}$ rapidly increases to values above $10^6 M_\odot$. For PBH masses close to and above $M_{\text{cr}}$ the Bondi accretion rate can be scaled by the Hubble viscosity loss given in the dashed curve in figure 3 (left) of [53].

Inserting $v_{\text{eff}}$ from equation (3.8) and figure 2 (right) into equation (3.11), assuming an accretion eigenvalue $\lambda=0.05$ and applying the above Hubble viscosity correction, I can finally calculate the normalized accretion rate as a function of redshift and PBH mass. The
results are shown in figure 3 (left). For PBH masses smaller than $\sim 1000 \, M_\odot$ the normalized accretion rate is roughly constant in the redshift range $20 < z < 200$ due to the fact that the density and velocity dependence on redshift in equation (3.9) roughly cancel out (see also the lower panel of figure 4 in [38]). At $z < 20$ $\dot{m}$ drops dramatically because of the effective velocity increase. PBH masses larger than $\sim 10^4 \, M_\odot$ reach accretion rates close to the Eddington limit at $z \gtrsim 100$, but are significantly affected by the Hubble viscosity at $z \gtrsim 20$. For all PBH masses the accretion rate is small enough, that the growth of the PBH population can be neglected over cosmic time (PBH with masses in the range $10^5-7 \, M_\odot$ accrete about $0.5-2\%$ of their mass until $z \gtrsim 20$).

4 Accretion spectrum and radiative efficiency

For the accretion flow and the electromagnetic emission mechanism I follow [8, 37] and assume the formation of an accretion disk. Accretion rates close to the Eddington limit will lead to the formation of a standard Shakura-Sunyaev disk [66], which has a canonical radiative efficiency $\eta \approx 0.1$. For much lower accretion rates $\dot{m} \ll 1$ an advection-dominated hot accretion flow [55] is expected, with a significantly lower radiation efficiency [56], roughly scaling according to $\eta \propto \dot{m}$. Figure 4 shows hot accretion flow spectra from [55] with a viscous heating parameter $\delta=0.5$ for black holes, normalized by Eddington luminosity and mass accretion rate. The left graph shows radiation from a $10 \, M_\odot$ black hole at different mass accretion rates. The right graph shows the spectrum from black holes with different masses in the range $10^{-6}-10^9 \, M_\odot$ and a mass accretion rate $\log(\dot{m}) = -1.6$.

It is important to understand, that for advection dominated accretion flows not all the matter entering the Bondi radius will actually reach the black hole. This is due to feedback mechanisms acting on the accreted gas, e.g. producing outflows or jets. The advection dominated flow models of [55, 56] therefore find a radial dependence of mass accretion rate $\dot{M} \propto R^\alpha$, typically with $\alpha \sim 0.4$. Within a radius of about $10 \, R_S$, where $R_S = 2GM/c^2$ is the Schwarzschild radius, the accretion flow more closely follows the standard Shakura-Sunyaev
description of a constant accretion rate with radius down to the last stable orbit ($\sim 3R_S$). In terms of the classical Bondi description of quasi-spherical capture, the loss of accreted matter can be associated with the accretion eigenvalue:

$$\lambda \approx \left( \frac{10R_S}{R_D} \right)^{\alpha}, \quad (4.1)$$

where $R_D$ is the outer radius of the accretion disk formed. For $\alpha=0.4$, the value of $\lambda=0.05$ chosen for the analysis in this paper therefore corresponds to an outer disk radius of $R_D \sim 2 \times 10^4 \, R_S$, about 8 orders of magnitude smaller than the Bondi radius. In this picture the accretion flow on large scales follows the Bondi quasi-spherical flow for most of the radial distance, until the advection-dominated accretion disk is formed.

The radiative efficiency for the ADAF spectra in figure 4 is the integral over these curves and has been calculated through numerical simulations by [56]. For this work I use a digitized version of the highest efficiency curve in their figure 1, with a viscous heating parameter $\delta=0.5$. $^1$ A maximum radiative efficiency of $\eta \sim 0.08$ is achieved for $\log(\dot{m}) > -1.6$. We can now calculate the radiative efficiency for every mass and redshift bin from the normalized accretion rate in figure 3 (left). The result is shown in figure 3 (right). It turns out that above redshifts $z \gtrsim 20$ and black hole masses $M_{PBH} > 100 \, M_\odot$, which dominate the contribution to the extragalactic background light, the radiative efficiencies are relatively large (typically $>3\%$).

We now have the ingredients to calculate the bolometric luminosity and flux expected from the baryon accretion onto the assumed PBH mass spectrum over cosmic time. For every black hole of mass $M_{PBH}$ I calculate the expected bolometric luminosity $L_{bol} = \dot{m} \eta L_{Edd}$, where $L_{Edd}=1.26 \times 10^{38} \, M_{PBH}/M_\odot \, \text{erg/s}$ is the Eddington luminosity, and the normalized

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$^1$Please take note that the definition of $\dot{m}$ between these authors and the analysis presented here differs by a factor of 10.
mass accretion rate $\dot{m}$ as well as the radiation efficiency $\eta$ are taken from the data in figure 3. In every mass bin, the relative number density of PBH compared to those of 1 M$_\odot$ is $n_{PBH} = f_{PBH}/M_{PBH}$, where $f_{PBH}$ is the PBH mass function from figure 1. For every mass and redshift bin I thus multiply the bolometric luminosity with this relative number density in order to obtain the density-weighted luminosity $\langle L_{bol}\rangle^*$ for an equivalent PBH of 1 M$_\odot$.

This quantity is shown in figure 5 as a function of PBH mass (left) and redshift (right). It shows that the largest contribution to the PBH luminosity over cosmic time comes from PBH in the mass range $M_{PBH} = 10^3-7$ at redshifts $z > 100$. The Chandrasekhar PBH mass peak is subdominant in this representation. The total PBH luminosity deposited in the baryonic gas at high redshifts is important for the pre-ionization and X-ray heating of the intergalactic medium discussed in section 6.

To calculate the contribution of PBH accretion to the extragalactic background light we need to convert the density-weighted luminosities in figure 5 to bolometric fluxes using the luminosity distance $D_L$ at the corresponding redshift: $\langle F_{bol}\rangle^* = \langle L_{bol}\rangle^*/(4\pi D_L^2)$. This quantity is shown in figure 6 as a function of PBH mass (left) and redshift (right). It shows that the largest contribution to the extragalactic surface brightness is produced at a redshift $z \approx 20$ from PBH in the mass range $M_{PBH} = 10^{2-5}$, and a similar contribution from the Chandrasekhar mass peak. SMBH at $M_{PBH} \sim 10^6.5$ have a notable contribution around $z \sim 10$.

5 The contribution of PBH to the extragalactic background light

To calculate the surface brightness per redshift shell in a particular observed frequency band $[\nu_1;\nu_2]$ of the electromagnetic spectrum, I take into account the spectral shape and the fraction of the radiation falling into the rest frame frequency band $[\nu_1/(1+z);\nu_2/(1+z)]$. The exact spectral shape is not so important for this derivation, it is mainly used to calculate the bolometric corrections, i.e. the fraction of the total luminosity falling into the various frequency bands as a function of redshift. The ADAF spectra in figure 4, in particular those at high $\dot{m}$ values, can be approximated by power laws with an exponential cutoff at $\sim 200$ keV. Follow-
Figure 6. Density-weighted bolometric flux of single PBH as a function of mass for different redshifts indicated (left), and as a function of redshift for different mass bins indicated (right).

I assume a power law slope of $-1$ (corresponding to a flat line in figure 4). Below a critical frequency $\nu_c$ the power law spectrum is cut off by synchrotron self-absorption into a power law with a steep slope of approximately $+1.86$. As can be seen in figure 4 (right), $\nu_c$ depends on $M_{PBH}$ and can be approximated by $\log(\nu_c) \approx 14.82 - 0.4 \log(M_{PBH}/M_\odot)$. The bolometric corrections are then obtained by integrating the analytic normalized spectra over the observed frequency bands. For the 2–5$\mu$m band we have to consider in addition the Lyman-$\alpha$ break, which produces a sharp cutoff at $z \gtrsim 30$ (see e.g. [28, 67]). These bolometric corrections are shown in figure 7 (left) for the 2–5$\mu$m NIR band, the 0.5–2 keV and the 2–10 keV X-ray bands, respectively.

To predict the surface brightness of all PBH across cosmic time in these observed frequency bands, the total flux per PBH in figure 6 (right) has to be multiplied with the bolometric correction and the PBH surface density in a particular redshift shell. Using the critical mass density of the universe $\rho_{\text{crit}} = 1.26 \times 10^{20} M_\odot \text{Gpc}^{-3}$ and the Dark Matter density $\Omega_{DM} = 0.264$, as well as the reference mass $1 M_\odot$, a comoving PBH space density of $n_{PBH} = 3.32 \times 10^{19} (1 + z)^3 \text{Gpc}^{-3}$ is obtained. For every redshift shell $[z+\Delta z]$ the PBH space density is multiplied with the volume of the shell $[V(z+\Delta z) - V(z)]$ and divided by $4\pi \text{deg}^2$ to obtain the number of PBH per deg$^2$. Figure 7 (right) shows the derived surface brightness as a function of redshift (per $\Delta z = 1$ interval) for the three spectral bands considered here. The emission in all three bands peaks around $z \approx 20$ with a FWHM of $\Delta z \approx [-3;+6]$.

The curves in figure 7 (right) can now be integrated to predict the total PBH contribution to the extragalactic background light as $SB_{2–5\mu m} \approx 10^{-13}$, $SB_{0.5–2\text{keV}} \approx 1.9 \times 10^{-13}$, and $SB_{2–10\text{keV}} \approx 1.3 \times 10^{-13} \text{erg cm}^{-2} \text{s}^{-1} \text{deg}^{-2}$, respectively. The minimum amount of X-ray surface brightness necessary to explain the CXB/CIB cross-correlation signal observed by [23] in the 0.5–2 keV band has been discussed by [29]. This is $9 \times 10^{-14} \text{erg cm}^{-2} \text{s}^{-1} \text{deg}^{-2}$, corresponding to roughly 1% of the total CXB signal in this band. The 0.5–2 keV PBH contribution predicted for an accretion eigenvalue of $\lambda = 0.05$ in equation (3.11) is thus about a factor of 2 larger than the observed CXB fluctuation signal, which could well be consistent, given the coherence between the CXB and CIB signals. As discussed above, there
Figure 7. Left: The bolometric correction, i.e. the fraction of the total luminosity falling into the respective observed frequency band as a function of redshift, for the 2–5µm NIR band, as well as the 0.5–2 and 2–10 keV X-ray bands. Right: Predicted surface brightness of the PBH in the same observed bands as a function of redshift (per ∆z=1).

is a marginally significant diffuse CXB remaining after accounting for all discrete source contributions \[31, 34\]. Extrapolating into the X-ray bands considered here, this residual flux corresponds to \(\approx (7 \pm 3)\) and \(\approx (9 \pm 20) \times 10^{-13} \text{ erg cm}^{-2} \text{ s}^{-1} \text{ deg}^{-2}\) in the 0.5–2 keV and 2–10 keV band, respectively. Assuming the \(\lambda=0.05\) value, the predicted PBH contribution is therefore well below the upper limit (15–25%) of any unresolved component left in the CXB. The main result of this paper is therefore, that the assumed PBH population for the dark matter can indeed explain the X-ray fluctuation signal, with a Bondi accretion eigenvalue of \(\lambda = 0.05\).

The flux measured in the 2–5µm CIB fluctuations at angular scales > 100” is about 1 nW m\(^{-2}\) sr\(^{-1}\) [68], or \(3 \times 10^{-10} \text{ erg cm}^{-2} \text{ s}^{-1}\). The cross-correlated CIB/CXB fluctuations contribute about 10% to the total CIB fluctuations \[23\], i.e. \(3 \times 10^{-11} \text{ erg cm}^{-2} \text{ s}^{-1}\). Therefore the predicted PBH contribution to these CIB fluctuations is only about 0.5% for \(\lambda=0.05\). It is argued in \[6\] that PBH in the early universe could amplify the cosmic power spectrum at small spatial scales (see below). Together with the pre-ionization of the intergalactic medium discussed below, the PBH can therefore significantly increase the associated star formation. The NIR emission in this picture would then be dominated by early star formation associated with PBH instead of direct PBH emission.

6 Discussion

6.1 Linear versus post-linear growth

In this simplified treatment I only consider the linear evolution of the power spectrum above the virialization redshift around \(z \approx 20\) (see figure 2 right). On sufficiently large scales the initial power spectrum has been very precisely determined as nearly scale invariant with overdensities of \(10^{-4}\) \[35\], and the PBH density field is expected to follow the standard adiabatic perturbations. On small scales the power spectrum is only poorly constrained and could be significantly amplified by the discrete nature of the PBH population itself \[6, 69, \]
Poisson variations in the density of PBH will introduce non-linear growth of density fluctuations and the corresponding velocity dispersion already well before the virialization redshift \( z \sim 20 \) discussed above. However, from numerical simulations \cite{70} conclude that the nonlinear velocity perturbations introduced by \( > 20 \, M_\odot \) PBH are too small to dominate the relative velocities between baryons and PBH at \( z \gtrsim 100 \) (see also \cite{71}). However, non-linear effects definitely become more important at lower redshifts (see above) and could effectively reduce the Bondi capture rate.

### 6.2 Magnetic fields in the early universe

The accretion mechanism assumed in the Bondi capture model only works, if there is a rough equipartition between the kinetic energy and magnetic fields in the accreted gas, as it is the case in the turbulent interstellar medium of our Galaxy. It is therefore justified to ask, whether this mechanism can also work at high redshifts, where the existence and magnitude of magnetic fields is still unclear. Magnetic fields are present at almost every scale of the low redshift universe, from stars and planets to galaxies and clusters of galaxies and possibly even in the intergalactic medium in voids of the cosmic web, as well as in high-redshift galaxies. \cite{72} and \cite{73} review the observations and possible origin of magnetic fields. There is a surprising similarity between the relatively strong magnetic fields measured in our own Galaxy (0.3–0.4 nT) and other nearby galaxies (\( \sim 1 \) nT) with magnetic fields measured in clusters of galaxies (0.1–1 nT), as well as in high redshift galaxies (\( \sim 1 \) nT), when the universe was only about 1/3 of its current age. There are even indications of magnetic fields of order \( \gtrsim 10^{-20} \) T in cosmic voids derived from the gamma ray emission of blazars \cite{74}.

One can come to the conclusion that the origin of cosmic magnetism on the largest scales of galaxies, galaxy clusters and the general intergalactic medium is still an open problem \cite{75}. It is usually assumed that primordial or cosmic seed fields are amplified over time through the galactic dynamo effect to produce the rather strong fields observed in local galaxies. In this picture it is, however, unclear how similar fields can be created in such different settings (e.g. clusters) and different cosmic times (high-redshift galaxies). An interesting possibility is therefore that cosmic magnetic fields could be remnants from the early universe, or created in a process without galactic dynamos. Assuming equipartition, the energy density in the CMB photons would correspond to a magnetic field of about 0.3 nT. Magnetic fields of \( 10^{-20} \) T, as observed in cosmic voids today, would only require a minute fraction of \( 10^{-10} \) of this energy density in the early universe to be channeled into magnetic fields.

Here I argue, that PBH could play a role in amplifying early magnetic seed fields and sustaining them until the epoch of galaxy formation. I compare the Bondi radius in eq. (3.12) and figure 8 (left) with the Larmor radius

\[
r_L = \frac{m v_\perp}{|q| B},
\]

which determines the gyro motion of particles moving through a magnetic field. Here \( m \) is the mass of the particle (either proton or electron), \( v_\perp \) is the velocity component of the particle perpendicular to the magnetic field, \( |q| \) is the absolute electric charge of the particle, and \( B \) is the magnetic field. Assuming a seed field of \( B=10^{-20} \) T and approximating the velocity with the sound speed \( v_\perp \approx c_s \) yields the gyro radius for both protons and electrons. The proton gyro radius is about a factor of 2000 larger than the electron gyro radius.

Figure 8 (left) shows the Bondi radius as well as the proton and electron Larmor radii as a function of redshift. If the gyro radius is smaller than the Bondi radius, the respective
Figure 8. Left: The Bondi radius for a $10^4 \, M_\odot$ (thin blue) and $1 \, M_\odot$ (thick blue) PBH compared to the proton (red) and electron (green) Larmor radius, assuming a magnetic field of $B=10^{-20} \, T$, as observed in local galaxy voids. Right: Baryon ionization/heating fraction $\chi_e$ as a function of redshift. The thin dash-dotted line shows the residual ionization left over from the radiation dominated era [76]. The red curve shows the ionization fraction from UV photons produced by accreting PBH. The blue curve shows the corresponding heating fraction by $>2$ keV X-ray photons. The thick dashed black line shows one of the models consistent with the Planck satellite data [35] (see text). The green hatched areas shows the range of high-redshift ionization fractions considered in [16].

A particle is easily accreted by the PBH. If, however, the gyro radius is larger than the Bondi radius, the particle will first not be easily accreted, but rather spiral around the PBH. From figure 8 we see, that at redshifts $z \gtrsim 70$ and PBH masses in the range $M_{PBH} \approx 0.3–500$ for our assumed magnetic field strength the proton Larmor radius is larger than the Bondi radius, while the electron Larmor radius is smaller than the Bondi radius. There is still a substantial fraction of residual electrons and protons/helium ions from the era before recombination (see the dash-dotted curve in figure 8 (right) from [76]). These electrons have therefore no problem being accreted, while for certain PBH masses protons resist the accretion. This will create a net electric current, which in turn will increase the average magnetic field strength until the proton gyro radius becomes smaller than the Bondi radius. This way the PBH can amplify the average magnetic field. The supersonic motion between baryon gas and PBH discussed above is expected to be coherent over large scales (of the order of Mpc) and can therefore induce large-scale ordered magnetic fields. A further magnetic field amplification occurs, as discussed above, in the accretion funnel, when magnetic fields are dissipated through reconnection and ejected with the plasma. In a sense, the ubiquitous PBH can possibly create their own magnetic field and distribute it throughout the universe. It is, however, plausible to assume, that magnetic fields in the early universe should be smaller than today, and the fractions of ionized baryons is less. This could also explain a rather small Bondi accretion eigenvalue required to match the observations.

6.3 Re-ionization

Next I turn to the contribution of PBH accretion to the re-ionization and re-heating history of the universe. At $z \approx 1089$, when the photons decoupled from the baryons and formed the
CMB radiation, the universe became predominantly neutral. Afterwards the universe entered a long period of “darkness”, in which the residual ionization left over from the primordial photon-baryon fluid diminished (see figure 8 right), the background photons cooled down, and any higher-frequency emission was quickly absorbed in the atomic gas. In the model described here the first sources to illuminate the “dark ages” would be the PBH accreting from the surrounding gas. Their ultraviolet emission, above the Hydrogen ionization energy of 13.6 eV, would start to re-ionize small regions around each PBH. However, in the beginning the density of the surrounding gas is still so high that the ionized matter quickly recombines. As long as the recombination time is much shorter than the Hubble time at the corresponding epoch, UV photons from the PBH cannot penetrate the surrounding medium, but instead produce an ionized bubble growing with time. In this type of ionization equilibrium the number of ionizing photons $N_{\text{ion}}$ required to overcome recombination is given as the ratio between the Hubble time $t_H(z)$ and the recombination time $t_{\text{rec}}(z)$ at the particular epoch, and can be derived from equations (2) and (3) in [77] as

$$N_{\text{ion}} = t_H / t_{\text{rec}} = \max \left[ 1, 0.59 \left( \frac{1+z}{7} \right)^{1.5} \right].$$

(6.2)

At a redshift $z=1000$, $N_{\text{ion}}$ is about 1000, and reaches a level of unity at $z \lesssim 10$ for the assumed set of parameters. For this calculation I ignore clumping of the ionized gas. In reality the effective clumping factor is relatively large for reionization at high redshift because the ionizing sources are more numerous in the filaments of the cosmic web, but must also ionize a correspondingly larger fraction of dense gas in the filaments, and thus ionization is slowed down. At lower redshift, when molecular gas and stars have already formed, not all UV photons will escape the dense regions. The effective escape fraction is one of the largest uncertainties in our current understanding of re-ionization. For simplicity, I assume an escape fraction $f_{\text{esc}}=0.1$ for UV photons, and $f_{\text{esc}}=1$ for X-ray photons, independent of redshift.

To calculate the history of pre-ionization by PBH I integrate the above normalized ADAF model for frequencies $\log(\nu)>15.52$ Hz, corresponding to the hydrogen ionization energy of 13.6 eV. To calculate the number of ionizing photons per PBH of reference mass 1 $M_\odot$ I take the density-weighted luminosity $\langle L_{\text{bol}} \rangle^*$ from figure 5 (right). To determine the average space density of ionizing photons I multiply with the average comoving space density of PBH (assuming the reference mass 1 $M_\odot$):

$$n_{\text{PBH}} = 1.06 \times 10^{-54} \left( \frac{1+z}{1000} \right)^3 \text{cm}^{-3},$$

(6.3)

and with the escape fraction $f_{\text{esc}}$ and finally divide by $N_{\text{ion}}$ from eq. (6.3) and the average density of baryons given in equation (2.10) to determine the ionization rate of baryons over cosmic time.

The red curve in figure 8 (right) shows the cumulative ionization fraction $\chi_e$ as a function of redshift for the accretion eigenvalue $\lambda=0.05$. A maximum cumulative ionization fraction of $\sim 2.8\%$, is reached at a redshift $z\approx 10$. This can be compared to one of the recent models determined from the Planck satellite data [35]. Here the 1$\sigma$ upper percentile of the FlexKnot model in their figure 45, which is consistent with the ionization optical depth determined from the most recent Planck data, is shown as dashed curve. A high-redshift contribution to the ionization history of the universe has also been discussed by [78] and [16]. The range of
values assumed in the latter work is shown as green hatched region in figure 8 (right). For
the choice of $\lambda=0.05$, the UV emission from the PBH population assumed in the toy model
is therefore fully consistent with the observational constraints from Planck.

6.4 X-ray heating

The role of X-ray heating in shaping the early universe has been discussed by [79]. Compared
to UV photons, X-ray photons have a much larger mean free path and can therefore ionize
regions far away from the source. In addition, most of the X-ray energy gets deposited into
heating up the gas. In order to estimate the amount of X-ray heating of the gas I applied the
same mechanism as for the UV photons above, but integrating the above ADAF model for
frequencies $\log(\nu) > 17.68$ Hz, corresponding to 2 keV. I assume an escape fraction of $f_{\text{esc}}=1$
and $N_{\text{ion}}=1$. The blue curve in figure 8 (right) shows the cumulative 2 keV heating fraction
per baryon as a function of redshift for the assumed accretion eigenvalue of $\lambda=0.05$. The
maximum cumulative heating fraction is $\sim 1.6\%$. X-rays from PBH therefore have only a
small contribution to the pre-ionization of the universe as a whole, but can be responsible
for a part of the pre-heating of gas observed in the ”entropy floor” of groups of galaxies. [80]
reviewed the energetics of groups and clusters of galaxies, which cannot be reproduced by
simple models, where the gas density is proportional to dark matter density. [81] and [82]
argued that the gas must have been pre-heated before falling into the cluster potential.
X-ray observations of groups of galaxies with ROSAT by [83] confirmed the need for a non-
gravitational entropy injection in the group gas. These authors coined the term “entropy
floor”, which amounts to an energy of about 2 keV per baryon injected into the group gas.
The pre-heating of the gas by PBH, albeit only contributing to a small fraction of the total
baryon content of the universe, could have played an important role in heating the high-
density regions, which first formed groups and clusters.

6.5 Cosmological 21-cm signal

The red-shifted 21-cm line can provide important new constraints on the physical processes
in the early universe [see e.g. 8, 84]. The Experiment to Detect the Global EoR Signature
(EDGES) has measured a strong, sky-averaged 21-cm absorption line profile after subtracting
the Galactic synchrotron emission [85]. The signal is centered at a frequency around 78 MHz
and covers a broad range in redshift $z=15–20$. The signal may be due to ultraviolet light
from first objects in the universe altering the emission of the 21-cm line by lowering the
spin temperature of neutral hydrogen relative to the CMB. However, the signal is about
time three larger than that expected from the standard ΛCDM cosmology, which led some
authors to suggest new dark matter physics [e.g. 86]. Instead of new physics, an increased
21-cm radio background contribution above the CMB at the epoch around $z=15–20$ could
also explain the EDGES signal. Indeed, [87] estimate the additional 21-cm radio background
from accretion onto putative radio-loud intermediate-mass black holes (IMBH) forming in
first molecular cooling halos at redshifts $z=16–30$. This could be sufficient to explain the
EDGES feature, however, it requires extreme assumptions about the radio loudness of the
IMBH population. Instead of assuming an interpretation in terms of mini-QSOs from IMBH
grown through accretion, I estimate here, whether PBH accretion could have a significant
contribution to the EDGES signal. A full treatment of this effect for the PBH toy model
is beyond the scope of this paper, but similar to the treatment of the PBH contribution to
the CXB and CIB derived in section 5, I can estimate the PBH contribution to the observed
low-frequency cosmic radio background, and thus to the EDGES signal.
The balloon-borne double-nulled Absolute Radiometer for Cosmology, Astrophysics and Diffuse Emission (ARCADE2) instrument has measured the absolute temperature of the sky at frequencies 3, 8, 10, 30, and 90 GHz, and detected a significant excess over the CMB blackbody spectrum at a temperature of 2.731 K [88]. Combining the ARCADE2 measurements with lower frequency data from the literature, the excess brightness temperature can be characterized as a power law $T = 1.19 \left(\frac{\nu}{1\ GHz}\right)^{-2.62} K$, which translates into a radio spectrum with a slope of $-0.62$ and a normalization of $3 \times 10^{-22} \text{ W m}^{-2} \text{ sr}^{-1}$ at 1.4 GHz. This cosmic radio synchrotron background is substantially larger than that expected from an extrapolation of the observed radio counts [89], and thus presents a major new challenge in astrophysics. [90] found that the global 21cm signal can be significantly amplified by an excess background radiation compared to the standard ΛCDM models, especially in absorption. Assuming that only 10% of the radio synchrotron background originates at large redshifts, they predict a 21cm feature almost an order of magnitude stronger than that expected purely from the CMB. Interpolating between their calculations for 0.1% and 10% excess background I find, that an excess high-redshift radiation field of about 5% of the observed radio synchrotron background is sufficient to explain the EDGES findings.

In order to calculate the expected PBH contribution to the radio background I assume that each black hole has a radio emission following the fundamental plane relation between X-ray luminosity, radio luminosity and black hole mass found by [91]. I use the parameterization for radio-quiet AGN from [92]: $\log(L_R) = 0.85 \log(L_X) + 0.12 \log(M_{PBH})$, where $L_R$ is the 1.4 GHz radio luminosity in units of $10^{40} \text{ erg/s}$, $L_X$ is the 0.1–2.4 keV X-ray luminosity in units of $10^{44} \text{ erg/s}$, and $M_{PBH}$ is the PBH mass in units of $10^8 M_\odot$. The X-ray luminosity is calculated from the bolometric luminosity shown in figure 5 (right). Assuming the ADAF radiation spectrum above, the fraction of the bolometric luminosity radiated in the 0.1–2.4 keV band is 0.23. For the radio spectrum I assume a power law with spectral index $-0.62$. This means that the bolometric correction is $\propto (1+z)^{0.38}$. The radio luminosities derived this way as a function of PBH mass and redshift are shown in figure 9. Multiplying these luminosities with the PBH density over cosmic time, converting into observed fluxes and integrating over mass and redshift I obtain a contribution of radio-quiet PBH to the observed radio background of $\sim 3 \times 10^{-25} \text{ W m}^{-2} \text{ sr}^{-1}$ at 1.4 GHz, i.e. a fraction of 0.1% of the observed synchrotron radio background. Most of this additional radiation field is accumulated at redshifts $z \gtrsim 20$. Following [90], this excess radio flux would increase the depth of the 21cm absorption line only by about 30%. If, however, some fraction of the PBH would be radio-loud (e.g. 5% with 1000 times higher fluxes), like observed in the AGN population, the 5% excess high-redshift radio background flux necessary to explain the EDGES feature could be easily achieved by PBH.

### 6.6 Primordial black holes in the galactic center

Next I discuss some observational effects of the putative PBH population residing in the Galactic Center region. First, assuming a Milky Way dark matter halo of $\sim 10^{12} M_\odot$, the PBH mass spectrum from section 2 (figure 1) indeed predicts about one supermassive PBH with a mass $\gtrsim 10^{6.5} M_\odot$, consistent with the Sgr A° SMBH in the center of our Galaxy [93]. To estimate the density of dark matter and baryons in the Galactic bulge region itself, I refer to dynamical models of the Milky Way’s center, using the density of red clump giant stars measured in infrared photometric surveys, as well kinematic radial velocity measurements of M-giant stars in the Galactic bulge/bar constructed in [94]. From N–body simulations of stellar populations for barred spiral discs in different dark matter halos these authors were able to determine with high precision the mass in a volume of $(\pm 2.2 \times \pm 1.4 \times \pm 1.2 \text{ kpc}^3)$
Density-weighted 1.4 GHz (observed) luminosity of a single PBH as a function of mass for different redshifts indicated.

Figure 9. Density-weighted 1.4 GHz (observed) luminosity of a single PBH as a function of mass for different redshifts indicated.

centered on the Galactic Bulge/Bar. The total mass is \((1.84\pm0.07)\times10^{10} \, M_\odot\). Depending on the assumed model, about 9–30% consists of dark matter, i.e. \(1.7–5.5\times10^9 \, M_\odot\). Applying the above PBH mass spectrum, we thus expect 5–10 intermediate-mass PBH with \(M_{PBH} > 10^4 \, M_\odot\) in the Galactic bulge region, but zero with \(M_{PBH} > 10^5 \, M_\odot\).

Recent high-resolution observations of high-velocity compact clouds (HVCC) in the central molecular zone of our Milky Way with the Atacama Large Millimeter/submillimeter Array (ALMA) have indeed identified five promising IMBH candidates, wandering through the patchy ISM in the Galactic Center (see [95]). The most compelling case is HCN-0.044-0.009, which shows two dense molecular gas streams in Keplerian orbits around a dark object with a mass \(M_{IMBH}=(3.2\pm0.6)\times10^4 \, M_\odot\) [96]. The semimajor axis of these Keplerian streams are around 2 and \(5\times10^{17} \, \text{cm}\). Another interesting case is the infrared and radio object IRS13E, a star cluster close to the Galactic Center potentially hosting an IMBH [97]. ALMA observations identified a rotating, ionized gas ring around IRS13E [98], with an orbit radius of \(6\times10^{15} \, \text{cm}\) and a rotation velocity of \(\sim230 \, \text{km/s}\). This is thus another promising IMBH candidate with a mass of \(M_{IMBH}=2.4\times10^4 \, M_\odot\).

Two of the five IMBH candidate sources in [95] are possibly associated with X-ray sources detected in the deep Chandra images of the Galactic Center [99]. IRS13E has the X-ray counterpart CXOGC 174539.7–290029 with an X-ray luminosity \(L_{2–10\,\text{keV}} \approx3\times10^{30} \, \text{erg/s}\), and CO–0.31+0.11 has the possible X-ray counterpart CXOGC 174426.3–290816 with an X-ray luminosity \(L_{2–10\,\text{keV}} \approx4\times10^{29} \, \text{erg/s}\). The other three sources have X-ray upper limits in the range of several \(10^{30} \, \text{erg/s}\). Assuming a bolometric correction factor of 1/30 for the 2–10 keV range, the combination of the mass accretion eigenvalue \(\lambda\) and the radiative efficiency \(\eta\) therefore has to be extremely small, on the order of \(3\times10^{-11}\). This is about a factor of 100 lower than the \(2\times10^{-9} \, L_{\text{Edd}}\) derived for the Galactic Center black hole Sgr A* [55]. Even assuming a very low efficiency ADAF model, a steady-state accretion solution is unlikely for these objects. The solution of this puzzle may come from the fact, that the velocity and density gradients of the gas in the Galactic Center region are so large, that the angular momentum forces any accreted matter into Keplerian motion well outside the classical Bondi radius (see [37]). Indeed, the orbital periods and lifetimes of the Keplerian
streams around HVCCs are in the range $10^{4}-5$ years, and thus accretion is expected to be highly variable on very long time scales. Another possibility to halt accretion for a considerable time is the feedback created by outflows during efficient accretion events. Numerical simulations of the gas dynamics in the center of the Galaxy [100] show that the outflows significantly perturb the gas dynamics near the Bondi radius and thus substantially reduce the capture rate. The net result of both these effects would be a highly variable, low duty cycle bursty accretion onto the IMBH and SMBH in the Galactic Center, consistent with the extremely low accretion efficiencies observed. The accretion limits for black holes in the mass range $M_{PBH}=20–100 \, M_{\odot}$ derived from deep Chandra and radio observations of the Galactic Center [45], are already shown in figure 1 to be consistent with the assumed PBH mass spectrum. Recent NuSTAR observations of the Galactic Center, including the effects of gas turbulence and the uncertainties related to the dark matter density profile even further weaken these constraints [101]. At any rate, the assumed PBH mass distribution of section 2 is fully consistent with the observational constraints for all PBH masses $> 20 \, M_{\odot}$ in the Galactic Center.

Finally, I check the PBH predictions for lower masses against the Galactic ridge X-ray emission (GRXE), an unresolved X-ray glow at energies above a few keV discovered almost 40 years ago and found to be coincident with the Galactic disk. The GRXE in the 2–10 keV band has a background-corrected surface brightness of $(7.1 \pm 0.5) \times 10^{-11} \, \text{erg} \, \text{cm}^{-2} \, \text{s}^{-1} \, \text{deg}^{-2}$ which was largely resolved into discrete sources [102], with the brightest source having an X-ray luminosity of about $10^{32} \, \text{erg} \, \text{s}^{-1}$, and the minimum detectable luminosity around $10^{30} \, \text{erg} \, \text{s}^{-1}$. The integrated emission has a strong iron line from hot plasma at 6.7 keV, and the authors interpret the X-ray emission as coming from a large population of cataclysmic variables and coronally active stars. Using the mass determination in the Galactic bulge/bar above I find that the average baryon density in this region is in the range $17–22 \, \text{cm}^{-3}$. However, most of these baryons are locked up in stars. In order to estimate the physical conditions of the gas in the Galactic Bulge/Bar region I follow [103]. According to these authors, there are four phases of the interstellar medium in the Galactic center region: (1) a cold molecular phase in Giant Molecular Clouds with temperatures around 50 K and gas densities $n=10^{4.5–4} \, \text{cm}^{-3}$ covering a volume fraction around 1%; (2) a warm molecular phase with temperatures around 150 K and gas density $n=10^{2.5} \, \text{cm}^{-3}$, covering a volume fraction of $\sim 10\%$; (3) an atomic phase with temperatures around 500–1000 K and density $\sim 10 \, \text{cm}^{-3}$, covering a volume fraction around 70%, and (4) ionized gas with temperatures $10^{4–8} \, \text{K}$ and an unknown density. Depending on the temperature of the interstellar medium, the sound speeds are in the range $c_{s}=1–100 \, \text{km/s}$. The stellar velocity dispersion in the central region of our Galaxy is in the range 100–140 km/s [104], while the dark matter velocity dispersion is about 110 km/s [105]. In the spirit of the discussion leading up to equation 3.9 and figure 2 (right) above, I assume an effective velocity for Bondi accretion $v_{\text{eff}} \approx 50 \, \text{km/s}$ and $\lambda=0.1$. As shown in figures 5 and 6, the PBH emissivity for the assumed mass spectrum is typically dominated by objects with $M_{PBH} > 100$, which already are discussed above. Indeed, calculating the Bondi accretion rates and radiative efficiencies for objects with $M_{PBH} < 100$ for the four ISM phases in the Galactic Center I obtain negligible PBH contributions to the total GRXE surface brightness. Some individual $M_{PBH} \sim 100 \, M_{\odot}$ objects in high density regions could in principle have X-ray luminosities up to $L_{2-10 \, \text{keV}}=10^{33} \, \text{erg/s}$, more luminous than the brightest X-ray source detected in the Galactic Ridge survey [102], but taking into account the strong variability and small duty cycle expected for this class of objects, their absence in the surveys is understandable. Some of the fainter unidentified sources in the current
deep X-ray surveys could indeed be accreting PBH and future large X-ray observatories like ATHENA [106] or LYNX [107] should be able to identify more.

7 Conclusions and outlook

The interpretation of cold dark matter as the sum of contributions of different mass PBH families [1] could explain a number of so far unsolved mysteries, like e.g. the massive seed black holes required to create the supermassive black holes in the earliest QSOs [13], the ubiquitous LIGO/VIRGO massive binary black holes (e.g. [6]), or even the putative "Planet X" PBH in our own Solar System [14]. The most abundant family of PBH should be around the Chandrasekhar mass (1.4 $M_\odot$). This prediction may already have been vindicated by the recent OGLE/GAIA discovery of a sizeable population of putative black holes in the mass range 1–10 $M_\odot$ [15]. Here I estimate the contribution of baryon accretion onto the overall PBH population to various cosmic background radiations, concentrating first on the cross-correlation signal between the CXB and the CIB fluctuations discovered in deep Chandra and Spitzer surveys [23]. Assuming Bondi capture and advection dominated disk accretion with reasonable parameters like baryon density and the effective relative velocity between baryons and PBH over cosmic time, as well as appropriate accretion and radiation efficiencies, I indeed predict a contribution of PBH consistent with the residual X-ray fluctuation signal. This signal peaks at redshifts $z \approx 17–30$. The PBH contribution to the 2–5 $\mu$m CIB fluctuations, however, is only about 1%, so that these would have to come from star formation processes associated with the PBH.

I discuss a number of other phenomena, which could be significantly affected by the PBH accretion. Magnetic fields are an essential ingredient in the Bondi accretion process, and I argue that the PBH can play an important role in amplifying magnetic seed fields in the early universe and maintaining them until the galactic dynamo processes set in. Next I study the contribution of the assumed PBH population to the re-ionization history of the universe and find that they do not conflict with the stringent ionization limits set by the most recent Planck measurements [35]. X-ray heating from the PBH population can provide a contribution to the entropy floor observed in groups of galaxies [83]. The tantalizing redshifted 21-cm absorption line feature observed by EDGES [85] could well be connected to the radio emission contributed by PBH to the cosmic background radiation. Finally, the number of IMBH and the diffuse X-ray emission in the Galactic Center region are not violated by the PBH dark matter, on the contrary, some of the discrete sources in the resolved GRXE could be accreting PBH.

It is obvious, that this simple PBH toy model for the dark matter requires significantly more work to turn it into quantitative predictions. Real magnetohydrodynamic simulations of the whole PBH mass spectrum including their own hierarchical clustering would be required to obtain the full history of their contribution to the cosmic backgrounds. The exciting EDGES discovery definitely requires a full-blown analysis of the radio contribution of PBH to the cosmic background. Future X-ray observations with eROSITA and ATHENA, infrared wide field surveys with Euclid and WFIRST, and microlensing observations with WFIRST will provide important additional diagnostics in this exciting and dramatically developing PBH field (see [108, 109]).
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References

[1] J. García-Bellido, Primordial black holes and the origin of the matter-antimatter asymmetry, Phil. Trans. Roy. Soc. A 377 (2019) 91.
[2] S. Hawking, Gravitationally collapsed objects of very low mass, Mon. Not. Roy. Astron. Soc. 152 (1971) 75 [inSPIRE].
[3] LIGO Scientific, Virgo collaboration, Binary black hole mergers in the first advanced LIGO observing run, Phys. Rev. X 6 (2016) 041015 [arXiv:1606.04856] [inSPIRE].
[4] LIGO Scientific, Virgo collaboration, Binary black hole population properties inferred from the first and second observing runs of advanced LIGO and advanced Virgo, Astrophys. J. Lett. 882 (2019) L24 [arXiv:1811.12940] [inSPIRE].
[5] S. Bird, I. Cholis, J.B. Muñoz, Y. Ali-Haïmoud, M. Kamionkowski, E.D. Kovetz et al., Did LIGO detect dark matter?, Phys. Rev. Lett. 116 (2016) 201301 [arXiv:1603.00464] [inSPIRE].
[6] A. Kashlinsky, LIGO gravitational wave detection, primordial black holes and the near-IR cosmic infrared background anisotropies, Astrophys. J. Lett. 823 (2016) L25 [arXiv:1605.04023] [inSPIRE].
[7] S. Clesse and J. García-Bellido, The clustering of massive Primordial black holes as dark matter: measuring their mass distribution with advanced LIGO, Phys. Dark Univ. 15 (2017) 142 [arXiv:1603.05234] [inSPIRE].
[8] O. Mena, S. Palomares-Ruiz, P. Villanueva-Domingo and S.J. Witte, Constraining the primordial black hole abundance with 21-cm cosmology, Phys. Rev. D 100 (2019) 043540 [arXiv:1906.07735] [inSPIRE].
[9] J. García-Bellido, B. Carr and S. Clesse, A common origin for baryons and dark matter, arXiv:1904.11482 [inSPIRE].
[10] C.T. Byrnes, M. Hindmarsh, S. Young and M.R.S. Hawkins, Primordial black holes with an accurate QCD equation of state, JCAP 08 (2018) 041 [arXiv:1801.06138] [inSPIRE].
[11] J. García-Bellido, Massive primordial black holes as dark matter and their detection with gravitational waves, J. Phys. Conf. Ser. 840 (2017) 012032 [arXiv:1702.08275] [inSPIRE].
[12] K.M. Belotsky, V.I. Dokuchaev, Y.N. Eroshenko, E.A. Esipova, M. Yu. Khlopin, L.A. Khromykh et al., Clusters of primordial black holes, Eur. Phys. J. C 79 (2019) 246 [arXiv:1807.06590] [inSPIRE].
[13] Y.-X. Li et al., Formation of z 6 quasars from hierarchical galaxy mergers, Astrophys. J. 665 (2007) 187 [astro-ph/0608190] [SPIRE].

[14] J. Scholtz and J. Unwin, What if Planet 9 is a primordial black hole?, arXiv:1909.11090 [SPIRE].

[15] L. Wyzykowski and I. Mandel, Constraining the mass of microlensing black holes and the mass gap with Gaia DR2, Astron. Astrophys. 636 (2020) A20 [arXiv:1904.07789] [SPIRE].

[16] A. Kashlinsky, R.G. Arendt, F. Atrio-Barandela, N. Cappelluti, A. Ferrara and G. Hasinger, Looking at cosmic near-infrared background radiation anisotropies, Rev. Mod. Phys. 90 (2018) 025006 [arXiv:1802.07774] [SPIRE].

[17] A. Kashlinsky, R.G. Arendt, J.C. Mather and S.H. Moseley, Tracing the first stars with fluctuations of the cosmic infrared background, Nature 438 (2005) 45 [astro-ph/0511105] [SPIRE].

[18] A. Kashlinsky, R.G. Arendt, J.C. Mather and S.H. Moseley, New measurements of cosmic infrared background fluctuations from early epochs, Astrophys. J. Lett. 654 (2007) L5 [Erratum ibid. 657 (2007) L131] [astro-ph/0612445] [SPIRE].

[19] R.G. Arendt, A. Kashlinsky, S.H. Moseley and J. Mather, Cosmic infrared background fluctuations in deep spitzer IRAC images: data processing and analysis, Astrophys. J. Suppl. 186 (2010) 10 [arXiv:0909.3816] [SPIRE].

[20] A. Kashlinsky, R.G. Arendt, M.L.N. Ashby, G.G. Fazio, J. Mather and S.H. Moseley, New measurements of the cosmic infrared background fluctuations in deep Spitzer/IRAC survey data and their cosmological implications, Astrophys. J. 753 (2012) 63 [arXiv:1201.5617] [SPIRE].

[21] T. Matsumoto, H.J. Seo, W.S. Jeong, H.M. Lee, S. Matsuura, H. Matsuhara et al., AKARI observation of the fluctuation of the near-infrared background, Astrophys. J. 742 (2011) 124 [arXiv:1010.0491] [SPIRE].

[22] K. Helgason, M. Ricotti and A. Kashlinsky, Reconstructing the Near-IR background fluctuations from known galaxy populations using multiband measurements of luminosity functions, Astrophys. J. 752 (2012) 113 [arXiv:1201.4398] [SPIRE].

[23] N. Cappelluti et al., Cross-correlating cosmic IR and X-ray background fluctuations: evidence of significant black hole populations among the CIB sources, Astrophys. J. 769 (2013) 68 [arXiv:1210.5302] [SPIRE].

[24] N. Cappelluti et al., Probing large scale coherence between Spitzer IR and Chandra X-ray source-subtracted cosmic backgrounds, Astrophys. J. Lett. 847 (2017) L11 [arXiv:1709.02824] [SPIRE].

[25] Y. Li, N. Cappelluti, R. G. Arendt, G. Hasinger, A. Kashlinsky and K. Helgason, The SPLASH and Chandra COSMOS Legacy Survey: the cross-power between near-infrared and X-ray background fluctuations, Astrophys. J. 864 (2018) 141 [arXiv:1807.10304].

[26] Y. Li, N. Cappelluti, G. Hasinger, R.G. Arendt, A. Kashlinsky and F. Pacucci, Spectral properties of populations behind the coherence in spitzer near-infrared and Chandra X-ray backgrounds, Astrophys. J. 883 (2019) 64, arXiv:1908.02293 [SPIRE].

[27] K. Helgason, N. Cappelluti, G. Hasinger, A. Kashlinsky and M. Ricotti, The contribution of z \leq 6 sources to the spatial coherence in the unresolved cosmic near-infrared and X-ray backgrounds, Astrophys. J. 785 (2014) 38 [arXiv:1311.1254] [SPIRE].

[28] B. Yue, A. Ferrara, R. Salvaterra, Y. Xu and X. Chen, Infrared background signatures of the first black holes, Mon. Not. Roy. Astron. Soc. 433 (2013) 1556 [arXiv:1305.5177] [SPIRE].
[29] A. Ricarte, F. Pacucci, N. Cappelluti and P. Natarajan, The clustering of undetected high-redshift black holes and their signatures in cosmic backgrounds, Mon. Not. Roy. Astron. Soc. 489 (2019) 1006 [arXiv:1907.03675].

[30] W.N. Brandt and G. Hasinger, Deep extragalactic x-ray surveys, Ann. Rev. Astron. Astrophys. 43 (2005) 827 [astro-ph/0501058] [inSPIRE].

[31] R.C. Hickox and M. Markevitch, Absolute measurement of the unresolved cosmic X-ray background in the 0.5-8 keV band with Chandra, Astrophys. J. 645 (2006) 95 [astro-ph/0512542] [inSPIRE].

[32] R.C. Hickox and M. Markevitch, Resolving the unresolved cosmic X-ray background in the Chandra deep fields, Astrophys. J. Lett. 661 (2007) L117 [astro-ph/0702556] [inSPIRE].

[33] L.L. Cowie, A.J. Barger and G. Hasinger, The faintest X-ray sources from z=0-8, Astrophys. J. 748 (2012) 50 [arXiv:1110.3326] [inSPIRE].

[34] N. Cappelluti et al., The Chandra COSMOS legacy survey: energy spectrum of the cosmic X-ray background and constraints on undetected populations, Astrophys. J. 837 (2017) 19 [arXiv:1702.01660] [inSPIRE].

[35] Planck collaboration, Planck 2018 results. VI. Cosmological parameters, arXiv:1807.06209 [inSPIRE].

[36] B. Carr, S. Clesse, J. García-Bellido and F. Kuhnel, Cosmic conundra explained by thermal history and primordial black holes, Phys. Rev. D 96 (2017) 043534 [arXiv:1612.05644] [inSPIRE].

[37] V. Poulin, P.D. Serpico, F. Calore, S. Clesse and K. Kohri, CMB bounds on disk-accreting massive primordial black holes, Phys. Rev. D 96 (2017) 083524 [arXiv:1707.04206] [inSPIRE].

[38] Y. Ali-Haımoud and M. Kamionkowski, Cosmic microwave background limits on accreting primordial black holes, Phys. Rev. D 95 (2017) 043534 [arXiv:1612.05644] [inSPIRE].

[39] M. Zumalacarregui and U. Seljak, Limits on stellar-mass compact objects as dark matter from gravitational lensing of type-IA supernovae, Phys. Rev. Lett. 121 (2018) 141101 [arXiv:1712.02240] [inSPIRE].

[40] Y. Ali-Haımoud, E.D. Kovetz and M. Kamionkowski, Merger rate of primordial black-hole binaries, Phys. Rev. D 96 (2017) 123523 [arXiv:1709.06576] [inSPIRE].

[41] F. Shankar, Black hole demography: from scaling relations to models, Class. Quant. Grav. 30 (2013) 244001 [arXiv:1307.3289] [inSPIRE].

[42] EROS-2 collaboration, Limits on the macho content of the galactic halo from the EROS-2 survey of the Magellanic clouds, Astron. Astrophys. 469 (2007) 387 [astro-ph/0607207] [inSPIRE].

[43] H. Niikura et al., Microlensing constraints on primordial black holes with Subaru/HSC Andromeda observations, Nat. Astron. 3 (2019) 524 [arXiv:1710.02151] [inSPIRE].

[44] LIGO Scientific, Virgo collaboration, Search for subsolar mass ultracompact binaries in advanced LIGO’s second observing run, Phys. Rev. Lett. 123 (2019) 161102 [arXiv:1904.08976] [inSPIRE].

[45] J. Manshanden, D. Gaggero, G. Bertone, R.M.T. Connors and M. Ricotti, Multi-wavelength astronomical searches for primordial black holes, JCAP 06 (2019) 026 [arXiv:1812.07967] [inSPIRE].

[46] A. Comastri, R. Gilli, A. Marconi, G. Risaliti and M. Salvati, Mass without radiation: Heavily obscured AGNs, the X-ray background and the black hole mass density, Astron. Astrophys. 574 (2015) L10 [arXiv:1501.03620] [inSPIRE].
[47] F. Hoyle and R.A. Lyttleton, The effect of interstellar matter on climatic variation, *Proc. Cambridge Phil. Soc.* **35** (1939) 405.

[48] H. Bondi and F. Hoyle, On the mechanism of accretion by stars, *Mon. Not. Roy. Astron. Soc.* **104** (1944) 273 [arXiv:0706.0864] [SPIRE].

[49] H. Bondi, On spherically symmetrical accretion, *Mon. Not. Roy. Astron. Soc.* **112** (1952) 195 [SPIRE].

[50] R.G. Edgar, A review of Bondi-Hoyle-Lyttleton accretion, *New Astron. Rev.* **48** (2004) 843 [arXiv:0709.0524] [SPIRE].

[51] V.F. Shvartsman, Halos around “Black Holes”, *Sov. Astron.* **15** (1971) 377.

[52] G.M. Beskin and S.V. Karpov, Low-rate accretion onto single stellar mass black holes, *Astron. Astrophys.* **440** (2005) 223 [arXiv:0403649] [SPIRE].

[53] M. Ricotti, Bondi accretion in the early universe, *Astrophys. J.* **662** (2007) 53 [arXiv:0706.0864] [SPIRE].

[54] M. Ricotti, J.P. Ostriker and K.J. Mack, Effect of primordial black holes on the cosmic microwave background and cosmological parameter estimates, *Astrophys. J.* **680** (2008) 829 [arXiv:0709.0524] [SPIRE].

[55] F. Yuan and R. Narayan, Hot accretion flows around black holes, *Ann. Rev. Astron. Astrophys.* **52** (2014) 529 [arXiv:1401.0586] [SPIRE].

[56] F.-G. Xie and F. Yuan, The Radiative Efficiency of Hot Accretion Flows, *Mon. Not. Roy. Astron. Soc.* **427** (2012) 1580 [arXiv:1207.3113] [SPIRE].

[57] S. Zaroubi, The epoch of reionization, *Astrophys. Space Sci. Lib.* **396** (2013) 45.

[58] R. Cen and J.P. Ostriker, Where are the baryons?, *Astrophys. J.* **514** (1999) 1 [astro-ph/9806281] [SPIRE].

[59] D. Tseliakhovich and C. Hirata, Relative velocity of dark matter and baryonic fluids and the formation of the first structures, *Phys. Rev. D* **82** (2010) 083520 [arXiv:1005.2416] [SPIRE].

[60] M. Ricotti, J.P. Ostriker and K.J. Mack, Effect of primordial black holes on the cosmic microwave background and cosmological parameter estimates, *Astrophys. J.* **680** (2008) 829 [arXiv:0709.0524] [SPIRE].

[61] V. Springel et al., Simulating the joint evolution of quasars, galaxies and their large-scale distribution, *Nature* **435** (2005) 629 [astro-ph/0504097] [SPIRE].

[62] W.A. Watson, I.T. Iliev, A. D’Aloisio, A. Knebe, P.R. Shapiro and G. Yepes, The halo mass function through the cosmic ages, *Mon. Not. Roy. Astron. Soc.* **433** (2013) 1230 [arXiv:1212.0095] [SPIRE].

[63] E. Munari, A. Biviano, S. Borgani, G. Murante and D. Fabjan, The relation between velocity dispersion and mass in simulated clusters of galaxies: dependence on the tracer and the baryonic physics, *Mon. Not. Roy. Astron. Soc.* **430** (2013) 2638 [arXiv:1301.1682] [SPIRE].

[64] N.I. Shakura and R.A. Sunyaev, Reprint of 1973A&A....24..337S. Black holes in binary systems. Observational appearance, *Astron. Astrophys.* **500** (1973) 33.

[65] M.R. Santos, V. Bromm and M. Kamionkowski, The contribution of the first stars to the cosmic infrared background, *Mon. Not. Roy. Astron. Soc.* **336** (2002) 1082 [astro-ph/0111467] [SPIRE].
[68] A. Kashlinsky, R.G. Arendt, J.C. Mather and S.H. Moseley, On the nature of the sources of the cosmic infrared background, Astrophys. J. Lett. 654 (2007) L1 [astro-ph/0612447] [inSPIRE].

[69] B. Carr and J. Silk, Primordial black holes as generators of cosmic structures, Mon. Not. Roy. Astron. Soc. 478 (2018) 3756 [arXiv:1801.00672] [inSPIRE].

[70] D. Inman and Y. Ali-Haïmoud, Early structure formation in primordial black hole cosmologies, Phys. Rev. D 100 (2019) 083528 [arXiv:1907.08129] [inSPIRE].

[71] G. Hüttsi, M. Raidal and H. Veermäe, Small-scale structure of primordial black hole dark matter and its implications for accretion, Phys. Rev. D 100 (2019) 083016 [arXiv:1907.06533] [inSPIRE].

[72] D. Grasso and H.R. Rubinstein, Magnetic fields in the early universe, Phys. Rept. 348 (2001) 163 [astro-ph/0009061] [inSPIRE].

[73] K. Subramanian, The origin, evolution and signatures of primordial magnetic fields, Rept. Prog. Phys. 79 (2016) 076901 [arXiv:1504.02311] [inSPIRE].

[74] K. Takahashi, M. Mori, K. Ichiki, S. Inoue and H. Takami, Lower bounds on magnetic fields in intergalactic voids from long-term GeV-TeV light curves of the Blazar Mrk 421, Astrophys. J. Lett. 771 (2013) L42 [arXiv:1303.3069] [inSPIRE].

[75] K. Subramanian, Magnetic fields in the universe, arXiv:1809.03543 [inSPIRE].

[76] M. Bruscoli, A. Ferrara and E. Scannapieco, How is the reionization epoch defined?, Mon. Not. Roy. Astron. Soc. 330 (2002) L43 [astro-ph/0201094] [inSPIRE].

[77] M. Ricotti and J.P. Ostriker, Reionisation, chemical enrichment and seed black holes from the first stars: is population III important?, Mon. Not. Roy. Astron. Soc. 350 (2004) 539 [astro-ph/0310331] [inSPIRE].

[78] C. Heinrich and W. Hu, Does Planck 2015 polarization data favor high redshift reionization?, Phys. Rev. D 98 (2018) 063514 [arXiv:1802.00791] [inSPIRE].

[79] A. Mesinger, A. Ferrara and D.S. Spiegel, Signatures of X-rays in the early Universe, Mon. Not. Roy. Astron. Soc. 431 (2013) 621 [arXiv:1210.7319] [inSPIRE].

[80] S. Dos Santos and O. Dore, Competition between shocks and entropy floor: unifying groups and clusters of galaxies, Astron. Astrophys. 383 (2002) 450 [astro-ph/0106456] [inSPIRE].

[81] N. Kaiser, Evolution of clusters of galaxies, Astrophys. J. 383 (1991) 104 [inSPIRE].

[82] A.E. Evrard and J.P. Henry, Expectations for X-Ray cluster observations by the ROSAT satellite, Astrophys. J. 383 (1991) 95.

[83] T.J. Ponman, D.B. Cannon and J.F. Navarro, The thermal imprint of galaxy formation on x-ray clusters, Nature 397 (1999) 135 [astro-ph/9810359] [inSPIRE].

[84] A. Fialkov and A. Loeb, Precise measurement of the reionization optical depth from the global 21-cm signal accounting for cosmic heating, Astrophys. J. 821 (2016) 59 [arXiv:1601.03058] [inSPIRE].

[85] A. Ewall-Wice, T.C. Chang, J. Lazio, O. Dore, M. Seiffert and R.A. Monsalve, Modeling the radio background from the first black holes at cosmic dawn: implications for the 21 cm absorption amplitude, Astrophys. J. 868 (2018) 63 [arXiv:1803.01815] [inSPIRE].
[88] D.J. Fixsen et al., *ARCADE 2 measurement of the extra-galactic sky temperature at 3–90 GHz*, *Astrophys. J.* **734** (2011) 5 [arXiv:0901.0555] [SPIRE].

[89] J. Singal et al., *The radio synchrotron background: conference summary and report*, *Publ. Astron. Soc. Pac.* **130** (2018) 036001 [arXiv:1711.09979] [SPIRE].

[90] C. Feng and G. Holder, *Enhanced global signal of neutral hydrogen due to excess radiation at cosmic dawn*, *Astrophys. J. Lett.* **858** (2018) L17 [arXiv:1802.07432] [SPIRE].

[91] A. Merloni, S. Heinz and T. Di Matteo, *A fundamental plane of black hole activity*, *Mon. Not. Roy. Astron. Soc.* **345** (2003) 1057 [astro-ph/0305261] [SPIRE].

[92] R. Wang, X.-B. Wu and M.-Z. Kong, *The black hole fundamental plane from a uniform sample of radio and x-ray emitting broad line agns*, *Astrophys. J.* **645** (2006) 890 [astro-ph/0603514] [SPIRE].

[93] R. Genzel, F. Eisenhauer and S. Gillessen, *The galactic center massive black hole and nuclear star cluster*, *Rev. Mod. Phys.* **82** (2010) 3121 [arXiv:1006.0064] [SPIRE].

[94] M. Portail, C. Wegg, O. Gerhard and I. Martinez-Valpuesta, *Made-to-measure models of the Galactic box/peanut bulge: stellar and total mass in the bulge region*, *Mon. Not. Roy. Astron. Soc.* **448** (2015) 713 [1502.00633].

[95] S. Takekawa, T. Oka, Y. Iwata, S. Tsujimoto and M. Nomura, *The fifth candidate for an intermediate-mass black hole in the galactic center*, *Astrophys. J.* **890** (2020) 167 [arXiv:2002.05173].

[96] S. Takekawa, T. Oka, Y. Iwata, S. Tsujimoto and M. Nomura, *Indication of another intermediate-mass black hole in the galactic center*, *Astrophys. J. Lett.* **871** (2019) L1 [arXiv:1812.10733].

[97] R. Schodel, A. Eckart, C. Iserlohe, R. Genzel and T. Ott, *A black hole in the galactic center complex IRS 13E?*, *Astrophys. J. Lett.* **625** (2005) L111 [astro-ph/0504474] [SPIRE].

[98] M. Tsuboi, Y. Kitamura, T. Tsutsumi, R. Miyawaki, M. Miyoshi and A. Miyazaki, *Rotating ionized gas ring around the Galactic center IRS13E3*, *Publ. Astron. Soc. Japan* **71** (2019) 105 [arXiv:1907.12311].

[99] M.P. Muno et al., *A catalog of X-ray point sources from two megaseconds of chandra observations of the galactic center*, *Astrophys. J. Suppl.* **181** (2009) 110 [arXiv:0809.1105] [SPIRE].

[100] J. Cuadra, S. Nayakshin and Q.D. Wang, *The role of feedback in accretion on low luminosity AGN: Sgr A* case study*, *Mon. Not. Roy. Astron. Soc.* **450** (2015) 277 [arXiv:1503.02745] [SPIRE].

[101] A. Hektor, G. Hütsi and M. Raidal, *Constraints on primordial black hole dark matter from Galactic center X-ray observations*, *Astron. Astrophys.* **618** (2018) A139 [arXiv:1805.06513] [SPIRE].

[102] M. Revnivtsev, S. Sazonov, E. Churazov, W. Forman, A. Vikhlinin and R. Sunyaev, *Discrete sources as the origin of the Galactic X-ray ridge emission*, *Nature* **458** (2009) 1142 [arXiv:0904.4649] [SPIRE].

[103] K. Ferriere, W. Gillard and P. Jean, *Spatial distribution of interstellar gas in the innermost 3 kpc of our Galaxy*, *Astron. Astrophys.* **467** (2007) 611 [astro-ph/0702532] [SPIRE].

[104] E. Valenti et al., *The central velocity dispersion of the Milky Way bulge*, *Astron. Astrophys.* **616** (2018) A83 [arXiv:1805.00275].

[105] P.M.W. Kalberla, J. Kerp and U. Haud, *The velocity dispersion of galactic dark matter*, *Astron. Soc. Pacific Conf. Series* **276** (2002) 453.
[106] K. Nandra et al., The hot and energetic universe: a white paper presenting the science theme motivating the Athena+ mission, arXiv:1306.2307 [INSPIRE].

[107] D.A. Schwartz et al., The Lynx X-ray observatory: revealing the invisible universe, in Proc. SPIE 11118 (2019) 111180K.

[108] A. Kashlinsky et al., Electromagnetic probes of primordial black holes as dark matter, arXiv:1903.04424 [INSPIRE].

[109] A. Kashlinsky et al., Probing the cross-power of unresolved cosmic infrared and X-ray backgrounds with upcoming space missions, Astrophys. J. Lett. 871 (2019) L6 [arXiv:1812.01535] [INSPIRE].

[110] E.L. Wright, A cosmology calculator for the world wide web, Publ. Astron. Soc. Pac. 118 (2006) 1711 [astro-ph/0609593] [INSPIRE].