Semantics of (Resilient) X10

Silvia Crafa¹ David Cunningham² Vijay Saraswat³ Avraham Shinnar³ Olivier Tardieu³

¹ University of Padova, Padova, IT
crafa@math.unipd.it
² Google, Inc
sparkprime@gmail.com
³ IBM TJ Watson Research Center
{vsaraswa,shinnar,tardieu}@us.ibm.com

Abstract. We present a formal small-step structural operational semantics for a large fragment of X10, unifying past work. The fragment covers multiple places, mutable objects on the heap, sequencing, try/catch, async, finish, and at constructs. This model accurately captures the behavior of a large class of concurrent, multi-place X10 programs. Further, we introduce a formal model of resilience in X10. During execution of an X10 program, a place may fail for many reasons. Resilient X10 permits the program to continue executing, losing the data at the failed place, and most of the control state, and repairing the global control state in such a way that key semantic principles hold, the Invariant Happens Before Principle, and the Failure Masking Principle. These principles permit an X10 programmer to write clean code that continues to work in the presence of place failure. The given semantics have additionally been mechanized in Coq.

1 Introduction

The need for scale-out programming languages is now well-established, because of high performance computing applications on supercomputers, and analytic computations on big data. Such languages – based for example on a partitioned global address space ([219], [10]) – permit programmers to write a single program that runs on a collection of places on a cluster of computers, can create global data-structures spanning multiple places, can spawn tasks at remote places, detect termination of an arbitrary tree of spawned tasks etc. The power of such languages is shown by programs such as M3R, which implement a high-performance, main-memory version of Hadoop Map Reduce [22] in a few thousand lines of code. Other high performance multi-place libraries have been developed for graph computations [12] and sparse matrix computations [23].

At the same time, the practical realities of running large-scale computations on clusters of commodity computers in commercial data centers are that nodes may fail (or may be brought down, e.g. for maintenance) during program executions. This is why multi-place application frameworks such as Hadoop [13], Resilient Data Sets [25], Pregel [18] and MillWheel [2] support resilient computations out of the box. In case of node failure, relevant portions of the user computation are restarted.
A new direction has been proposed recently in [11]: extending a general purpose object-oriented, scale-out programming language (X10) to support resilience. The hypothesis is that application frameworks such as the ones discussed above can in fact be programmed in a much simpler and more direct fashion in an object-oriented language (powerful enough to build parallel, distributed libraries) that already supports resilience. It is feasible to extend X10 in this way since is based on a few, orthogonal constructs organized around the idea of places and asynchrony. A place (typically realized as a process) is simply a collection of objects together with the threads that operate on them. A single computation may have tens of thousands of places. The statement async $S$ supports asynchronous execution of $S$ in a separate task. finish $S$ executes $S$, and waits for all tasks spawned by $S$ to terminate. Memory locations in one place can contain references (global refs) to locations at other places. To use a global ref, the at (p) $S$ statement must be used. It permits the current task to change its place of execution to p, execute $S$ at p and return, leaving behind tasks that may have been spawned during the execution of $S$. The termination of these tasks is detected by the finish within which the at statement is executing. The values of variables used in $S$ but defined outside $S$ are serialized, transmitted to p, de-serialized to reconstruct a binding environment in which $S$ is executed. Constructs are provided for unconditional (atomic $S$) and conditional (when (c) $S$) atomic execution. Finally, Java-style non-resumptive exceptions (throw, try/catch) are supported. If an exception is not caught in an async, it is propagated to the enclosing finish statement. Since there may be many such exceptions, they appear wrapped in a MultipleExceptions exception.

[11] shows that this programming model may be extended to support resilience in a surprisingly straightforward way. A place p may fail at any time with the loss of its heap and tasks. Any executing (or subsequent) tasks on that place throw a DeadPlaceException (DPE). Global refs pointing to locations hosted at p now “dangle”; however they can only be dereferenced via an at (p) $S$, and this will throw a DPE exception. If a task at a failed place has started a task $T$ at another place, this task is not aborted. Instead Resilient X10 posits a high level principle, the Happens Before Invariance (HBI) principle: Failure of a place should not alter the happens before relationship between statement instances at remaining places. [11] shows that many interesting styles of resilient programming can be expressed in Resilient X10. The language is implemented at fairly modest cost.

In this paper we formalize the semantics of Resilient X10. Our fundamental motivation is to provide a mechanized, formal semantics for a core fragment of Resilient X10 that is separate from the implementation and can be used as a basis for reasoning about properties of programs and for establishing that principles such as HBI actually hold.

We proceed as follows. Our first task is to formalize a large portion of X10. We build on the small-step, transition system for X10 presented in [24] which deals with finish, async and for loops. We extend it to handle multiple places and at, exceptions and try/catch statements, necessary to express place failure. (In the spirit of [24] we omit formalization of any of the object-oriented features of X10 since it is fairly routine.) Configurations are just pairs $<s, g>$ representing a statement $s$ (the program to be executed) and a global heap $g$, a partial map from the set of places to heaps. Transitions are (potentially) labeled with exceptions, tagged with whether they were generated.
from a synchronous or asynchronous context. We establish desirable properties of the transition system (absence of stuck states, invariance of place-local heaps). We establish a bisimulation based semantics that is consistent with the intuitions underlying the “gap based” trace set semantics of Brookes [8]. We establish a set of equational laws for this semantics.

On this foundation we show that the semantics of Resilient X10 can be formalized with just three kinds of changes. (1) A place failure transition models the failure of a place $p$ by simply removing $p$ from the domain of $g$. This cleanly models loss of all data at $p$. Next, the transition rules for various language constructs are modified to reflect what happens when those constructs are “executed” at a failed place. (2) An attempt to activate any statement at a failed place results in a DeadPlaceException (abbreviated henceforth as DPE). (3) Consistent with the design of Resilient X10, any exceptions thrown by (the dynamic version of) an at($q$) s at a failed place $q$ are masked by a DPE. These are the only changes needed.

We show that the main properties of TX10 carry over to Resilient TX10. We also show important resilience-related properties. Our main theorem establishes that in fact Resilient TX10 satisfies Happens Before Invariance. We also present a set of equational laws and discuss differences with the laws for TX10.

We have encoded a mechanized version of the syntax and semantics of both TX10 and Resilient X10 in Coq, an interactive theorem prover [4]. In doing so we addressed the challenge of formalizing the copy operation on heaps and establishing termination (even in the presence of cycles in the object graph). We mechanize the proof that there are no stuck configurations, and furthermore prove that the relation is computable, yielding a verified interpreter for TX10 and Resilient X10.

Related work. Our work is related to three broad streams of work. The first is formalization of X10 and Java with RMI. The first formalization of X10 was in [21]. This paper adapts the framework of Middleweight Java [5] to represent a configuration as a collection of stacks and heaps. This choice led to a rather complex formalization. [17] presents an operational semantics for the X10 finish/async fragment, but again with a complex representation of control. We build on the work of [24] which for the first time represents the control state as a statement, and presents a very simple definition of the Happens Before relation. We extend that work to handle exceptions (necessary for the formalization of resilience), and place-shifting at, and formally treat resilience. [1] presents a semantics for Java with remote method invocation; hence they also deal with multiple places and communication across places. In particular they formalize a relational definition of copying an object graph, although they do not formalize or mechanize an implementation of this specification. Their formalization does not deal with place failure, since Java RMI does not deal with it.

The second stream is the work on formalization of the semantics of concurrent imperative languages [7,6,8]. Our work can be seen as adding block-structured concurrency constructs (finish, async), exceptions, and, of course, dealing with multiple places, and place failure.

The third stream is the work on distributed process algebras that deal with failure [14,16,15,3,19]. [3] introduces an extension of the π-calculus with located actions, in the context of a higher-order, distributed programming language, Facile. [14] introduces
locations in the distributed join calculus, mobility and the possibility of location failure, similar to our place failure. The failure of a location can be detected, allowing failure recovery. In the context of Dπ [16], an extension of the π-calculus with multiple places and mobility, [15] gives a treatment of node- and link-failure. In relationship with all these works, this work differs in dealing with resilience in the context of distributed state, global references, mobile tasks with distributed termination detection (finish), and exceptions, and formalizing the HBI principle. Our work is motivated by formalizing a real resilient programming language, rather than working with abstract calculii.

Summary of Contributions. The contributions of this paper are:

- We present a formal operational semantics for significant fragment of X10, including multiple places, mutable heap, try/catch statements, throws, async, finish and at statements. The semantics is defined in terms of a labeled transition relation over configurations in which the control state is represented merely as a statement, and the data state as a mapping from places to heaps.
- We present a set of equational laws for operational congruence.
- We extend the formal operational semantics to Resilient X10, showing that it enjoys Happens Before Invariance and Failure Masking Principles.
- We present equational laws for Resilient X10.
- We mechanize proofs of various propositions in Coq. In particular, the proof that no configurations are stuck yields a verified executable version of the semantics.

Rest of this paper. Section 2 introduces TX10, informally describing the basic constructs and a small-step operational semantics of TX10. Section 3 presents laws for equality for a semantics built on congruence over bisimulation. The second half of the paper presents a semantic treatment of resilience. Section 4 discusses the design of Resilient X10, formalizes the semantics, and presents equational laws for congruence. Section 5 concludes.

2 TX10

We describe in this section the syntax and the semantics of TX10, the formal subset of the X10 language [20] we consider in this work. We have also encoded a mechanized version in Coq, which will be discussed in Section 2.2.

The syntax of TX10 is defined in Table 1. We assume an infinite set of values Val, ranged over by \( v, w \), an infinite set of variables ranged over by \( x, y \), and an infinite set of field names ranged over by \( f \). We also let \( p, q \) range over a finite set of integers \( \mathbb{P} = \{0\ldots(n-1)\} \), which represent available computation places. A source program is defined as a static statement \( s \) activated at place 0 under a governing finish construct. The syntax then includes dynamic statements and dynamic values that can only appear at runtime. Programs operate over objects, either local or global, that are handled through object identifiers (object ids). We assume an infinite set of object ids, \( \text{ObjId} \) (with a given bijection with the natural numbers, the “enumeration order”); objects are in a one to one correspondence with object ids. Given the distributed nature of the language and to model X10’s GlobalRef, we assume that each object lives in a specific (home)
place, and we distinguish between local and global references. More precisely, we use
the following notation:

- \( p : \text{ObjId} \rightarrow \text{Pl} \) maps each object id to the place where it lives;
- \( \text{ObjId}_q = \{ o \in \text{ObjId} \mid p(o) = q \} \) and \( \text{grObjId} = \{ o@p \mid o \in \text{ObjId}_p \land p \in \text{Pl} \} \)

Then given \( o \in \text{ObjId}_q \), we say that \( o \) is a local reference (to a local object) while \( o@q \) is a global reference (to an object located at \( q \)).

The expression \( \{ f_1 : e_1, \ldots, f_n : e_n \} \) (for \( n \geq 0 \)) creates a new local object and returns its fresh id. The object is initialized by setting, in turn, the fields \( f_i \) to the value obtained by evaluating \( e_i \). Local objects support field selection: the expression \( e.f \) evaluates to the value of the field with name \( f \) in the object whose id is obtained by evaluating \( e \). Similarly, the syntax of statements allows field update. X10 relies on a type system to ensure that any selection/update operation occurring at runtime is performed on an object that actually contains the selected/updated field. Since TX10 has no corresponding static semantic rules, we shall specify that \( o.f \) throws a BadFieldSelection BF exception when the object \( o \) does not have field \( f \).

The expression \( \text{globalref} e \) creates a new global reference for the reference returned by the evaluation of \( e \). Whenever \( e \) evaluates to a global reference, the expression \( \text{valof} e \) returns the local object pointed by the reference. Errors in dealing with global references are handled explicitly.
references are modelled by throwing a $\text{BadGlobalRef}$ exception $BG$. (see Section 2.1 for a detailed explanation of the semantics of global references).

TX10 deals with exception handling in a standard way: the statement $\text{throw } v$ throws an exception value $v$ that can be caught with a $\text{try catch } t$ statement. For simplicity, exception values are constants: besides $BF$ and $BG$ described above, we add $E$ to represent a generic exception. The exception $DP$ stands for $\text{DeadPlaceException}$, and will only appear in the semantics of the resilient calculus in Section 4. Variable declaration $\text{val } x = e s$ declares a new local variable $x$, binds it to the value of the expression $e$ and continues as $s$. The value assigned to $x$ cannot be changed during the computation. We shall assume that the only free variable of $s$ is $x$ and that $s$ does not contain a sub-statement that declares the same variable $x$. This statement is a variant of the variable declaration available in X10. In X10 the scope $s$ is not marked explicitly; rather all statements in the rest of the current block are in scope of the declaration. We have chosen this “let” variant to simplify the formal presentation.

The construct $\text{async } s$ spawns an independent lightweight thread, called $\text{activity}$, to execute $s$. The new activity running in parallel is represented by the dynamic statement $\text{async } s$. The statement $\text{finish } s$ executes $s$ and waits for the termination of all the activities (recursively) spawned during this execution. Activities may terminate either normally or abruptly, i.e. by throwing an exception. If one or more activities terminated abruptly, $\text{finish } s$ will itself throw an exception that encapsulates all exceptions. In TX10, we use the parameter $\mu$ in $\text{finish } s$ to record the exception values thrown by activities in $s$. $\mu$ is a possibly empty set of values; we simply write $\text{finish } s$ instead of $\text{finish } \emptyset s$.

The sequence statement $\{ s t \}$ executes $t$ after executing $s$. Note that if $s$ is an $\text{async}$, its execution will simply spawn an activity $\text{async } s$, and then activates $t$. Therefore, $\{ \text{async } s \ t \}$ will actually represent $s$ and $t$ executing in parallel. We say that sequencing in X10 has shallow $\text{finish}$ semantics.

Finally, $\text{at}(p)(\text{val } x = e) s$ is the place-shifting statement. We assume that the only free variable in $s$ is $x$. This statement first evaluates $e$ to a value $v$, then copies the object graph rooted at $v$ to place $p$ to obtain a value $v'$, and finally executes $s$ synchronously at $p$ with $x$ bound to $v'$. Running $s$ at $p$ synchronously means that in $\{ \text{at}(p)(\text{val } x = e) s \ t \}$, $t$ will be enabled precisely when the $\text{at}$ statement has only asynchronous sub-statements left (if any). Thus $\text{at}$ also has shallow $\text{finish}$ semantics, just like sequential composition. In some cases the programmer may not need to transmit values from the calling environment to $s$, the variant $\text{at } (p) s$ may be used instead. As an example, the program $\text{finish at}(0) \{ \text{at}(1) \text{async } s \ \text{at}(2) \text{async } s \}$ evolves to a state where two copies of $s$ run in parallel at places 1 and 2. The entire program terminates whenever both remote computations end.

Currently, X10 supports a variant of these $\text{at}$ constructs. The programmer writes $\text{at } (p) s$ and the compiler figures out the set of variables used in $s$ and declared outside $s$. A copy is made of the object reference graph with the values of these variables as roots, and $s$ is executed with these roots bound to this copied graph. Moreover X10, of course, permits mutually recursive procedure (method) definitions. We leave the treatment of recursion as future work.
2.1 Operational Semantics

We build on the semantics for X10 presented in [24]. In this semantics, the data state is maintained in a shared global heap (one heap per place), but the control state is represented in a block structured manner – it is simply a statement.

\[
\text{Heap } h ::= \emptyset | h \cdot [o \mapsto v] \\
\text{Global heap } g ::= \emptyset | g \cdot [p \mapsto h]
\]

The local heap at a place \( p \) is a partial map that associates object ids to objects represented by partial maps \( r \) from field names to object ids. The global heap \( g \) is a partial map from the set of places \( \mathcal{P} \) to local heaps. We let \( \emptyset \) denote the unique partial map with empty domain, and for any partial map \( f \) by \( f[p \mapsto v] \) we mean the map \( f' \) that is the same as \( f \) except that it takes on the value \( v \) at \( p \). Moreover, in the following we write \( s[v/x] \) for variable substitution.

X10 is designed so that at run-time heaps satisfy the place-locality invariant formalized below. Intuitively, the domain of any local heap only contains local object references, moreover any object graph (rooted at a local object) only contains references to either (well defined) local objects or global references.

Let \( h \) be a local heap and \( o \in \text{dom}(h) \) an object identifier. We let \( h \downarrow o \) denote the object graph rooted at \( o \), that is the graph with vertexes the values reachable from \( o \) via the fields of \( o \) or of one or more intermediaries. In other terms, it is the graph where an \( f \)-labelled edge \((v, f, v')\) connects the vertexes \( v \) and \( v' \) whenever \( v \) is an object with a field \( f \) whose value is \( v' \). We also denote by \( h_o \) the set of all object values that are reachable from \( o \), that is the set of all vertexes in the object graph \( h \downarrow o \).

**Definition 2.1 (Place-local heap).** A global heap \( g \) is place-local whenever for every \( q \in \text{dom}(g) \), and \( h = g(q) \)

\[\text{dom}(h) \subseteq \text{ObjId}_q \text{ and } \forall o \in \text{dom}(h). \ h_o \subseteq (\text{ObjId}_q \cap \text{dom}(h)) \cup \text{grObjId}\]

The semantics is given in terms of a transition relation between configurations, which are either a pair \( \langle s, g \rangle \) (representing the statement \( s \) to be executed in global heap \( g \)) or a singleton \( g \), representing a computation that has terminated in \( g \). Let \( k \) range over configurations. The transition relation \( k \xrightarrow{\lambda} \ k' \) is defined as a labeled binary relation on configurations, where \( \lambda \in \mathcal{L} = \{ \epsilon, v \times, v \otimes \} \), and \( p \) ranges over the set of places. The transition \( k \xrightarrow{\lambda} \ k' \) is to be understood as: the configuration \( k \) executing at \( p \) can in one step evolve to \( k' \), with \( \lambda = \epsilon \) indicating a normal transition, and \( \lambda = v \otimes \), resp. \( v \times \), indicating that an exception has thrown a value \( v \) in a synchronous, resp. asynchronous, subcontext. Note that failure is not fatal; a failed transition may be followed by any number of failed or normal transitions. We shall write \( \xrightarrow{\epsilon} \) as \( \xrightarrow{} \).

**Definition 2.2 (Semantics).** Let \( \xrightarrow{} \) represent the reflexive, transitive closure of \( \xrightarrow{\lambda} \).

The operational semantics, \( \mathcal{O}[s] \) of a statement \( s \) is the relation

\[
\mathcal{O}[s] \overset{\text{def}}{=} \{(g, g') \mid \langle \text{finish } \pi \rangle (0) s, g) \xrightarrow{} g'\}
\]
⊢ isAsync async s
⊢ isAsync async (p) s
⊢ isAsync try s catch t
⊢ isAsync t
⊢ isAsync { s t }

⊢ isSync s

⊢ isSync s

⊢ isSync s

⊢ isSync s

⊢ isSync{ s t }
⊢ isSync { t s }
⊢ isSync async s
⊢ isSync finish µ s, throw v

Table 2. Synchronous and Asynchronous Statements

In order to present rules compactly, we use the “matrix” convention exemplified below, where we write the left-most rule to compactly denote the four rules obtained from the right-most rule with i = 0, 1, j = 0, 1.

\[
\begin{array}{c}
\gamma \xrightarrow{\lambda} \gamma_0 | \gamma_1 \\
\text{cond}_0 \delta^0 \xrightarrow{\lambda_0} \delta_0^0 | \delta_0^1 \\
\text{cond}_1 \delta^1 \xrightarrow{\lambda_1} \delta_1^0 | \delta_1^1
\end{array}
\]

\[
\begin{array}{c}
\gamma \xrightarrow{\lambda} \gamma_i \text{ cond}_j \\
\delta^i \xrightarrow{\lambda_j} \delta^j_i \\
i = 0, 1 \ j = 0, 1
\end{array}
\]

We also introduce in Table 2 two auxiliary predicates to distinguish between asynchronous and synchronous statements. A statement is asynchronous if it is an async s, or a sequential composition of asynchronous statements (possibly running at other places). The following proposition is easily established by structural induction.

**Proposition 2.3.** For any statement s, either ⊢ isAsync s xor ⊢ isSync s.

In order to define the transition between configurations, we first define the evaluation relation for expressions by the rules in Table 3. Transitions of the form \(\langle e, h \rangle \xrightarrow{p} \langle e', h' \rangle\) state that the expression e at place p with local heap h correctly evaluates to e' with heap h'. On the other hand an error in the evaluation of e is modeled by the transition \(\langle e, h \rangle \xrightarrow{v} p\). An object creation expression is evaluated from left to right, according to rule (E XP C TX). When all expressions are evaluated, rule (N EW OBJ) states that a new local object id is created and its fields set appropriately. Rule (N EW GLOBAL) shows that a new global reference is built from an object id o by means of the expression `globalref o`. A global reference o$p can be dereferenced by means of the valof expression. Notice that rule (VALOF), according to X10’s semantics, shows that the actual object can only be accessed from its home place, i.e. p(o) = p. Any attempt to select a non-existing field from an object results in the BF exception by rule (SELECT BAD), while any attempt to access a global object that is not locally defined result in a BG error by rule (VALOF BAD). In X10, the static semantics guarantees that objects and global references are correctly created and that any attempt to select a filed is type safe, hence well typed X10 programs do not occur in BF and BG exceptions, however we introduce rules (SELECT BAD), (VALOF BAD) and (BAD FIELD UPDATE) so that
The operational semantics of TX10 enjoys the property that there are no stuck states, i.e. Proposition 2.7 in Section 2.3.

The following proposition shows that the heap modifications performed by rules (NEW OBJ) and (NEW GLOBAL REF) respect the place-locality invariant.

**Proposition 2.4.** Let \( g \) be a place-local heap, \( p \in \text{dom}(g) \) and \( h = g(p) \). We say that \( \langle e, h \rangle \) is place-local whenever for any local object id \( o \) occurring in \( e \) it holds \( o \in \text{dom}(h) \). If \( \langle e, h \rangle \) is place-local and \( \langle e, h \rangle \xrightarrow{p} \langle e', h' \rangle \), then \( g \cdot \{ p \mapsto h' \} \) is place-local, and \( \langle e', h' \rangle \) is place-local.

Now we turn to the axiomatization of the transition relation between configurations.

Table 3 collects a first set of rules dealing with basic statements. These rules use the condition \( p \in \text{dom}(g) \), which is always true when places do not fail. We include this condition to permit the rules of Table 4 to be reused when we consider place failure in Section 4. Most of these rules are straightforward. Rule (EXCEPTION) shows that throwing an exception is recorded as a synchronous failure. Moreover, rule (BAD FIELD UPDATE) throws a BF exception whenever \( f \) is not one of its fields.

The rest of operational rules are collected in Table 5. These rules, besides defining the behavior of the major X10 constructs, also illustrate how the exceptions are propagated through the system and possibly caught. The \texttt{async} construct takes one step to spawn the new activity. Moreover, according to rule (SYNC), an exception (either
synchronous or asynchronous) in the execution of s is masked by an asynchronous exception in async s. Asynchronous failures are confined within the thread where they originated, and they are caught by the closest finish construct that is waiting for the termination of such a thread. More precisely, the finish s statement waits for the termination of any (possibly remote) asynchronous (and synchronous as well) activities spawned by s. Any exception thrown during the evaluation of s is absorbed and recorded into the state of the governing finish. Indeed, consider rule (FINISH) where we let be $\mu \cup \lambda = \mu$ if $\lambda = \varepsilon$ and $\mu \cup \lambda = \{v\} \cup \mu$ if $\lambda = v \times$ or $\lambda = v \otimes$. Then this rule shows that the consequence has a correct transition $\rightarrow_p$, even when $\lambda \neq \varepsilon$: i.e., the exception in s has been absorbed and recorded into the state of finish. Moreover, the rule (END OF FINISH) shows that finish terminates with a generic synchronous exception whenever at least one of the activities its governs threw an exception (in X10 it throws a MultiplexExceptions containing the list of exceptions collected by finish). Two rules describe the semantics of sequential composition. When executing \{s t\}, rule (SEQ) shows that the continuation t is activated whenever s terminates normally or with an asynchronous exception. On the other hand, when the execution of s throws a synchronous exception (possibly leaving behind residual statements s') the continuation t is discarded. Rule (PAR) captures the essence of asynchronous execution allowing reductions to occur in parallel components.

The rule (PLACE SHIFT) activates a remote computation; it uses a copy operation on object graphs, copy(o, q, g), that creates at place q a copy of the object graph rooted at o, respecting global references. In X10 place shift is implemented by recursively serializing the object reference graph G rooted at o into a byte array. In this process, when it is encountered a global object reference o\$p, the fields of this object are not followed; instead the unique identifier o\$p is serialized. The byte array is then transported.
to \( q \), and de-serialized at \( q \) to create a copy \( G' \) of \( G \) with root object a fresh identifier \( o' \in \text{ObjId}_q \). All the objects in \( G' \) are new. \( G' \) is isomorphic to \( G \) and has the additional property that if \( z \) is a global ref that is reachable from \( o \) then it is also reachable (through the same path) from \( o' \).

**Definition 2.5 (The copy operation.)** Let \( g \) be a global heap, \( q \) a place with \( h = g(q) \). Let \( o \in \text{ObjId} \) such that \( p(o) \in \text{dom}(g) \), then \( \text{copy}(o, q, g) \) stands for the (unique) tuple \( \langle o', g[q \rightarrow h'] \rangle \) satisfying the following properties, where \( N = \text{dom}(h') \setminus \text{dom}(h) \).

- \( N \) is the next \( |N| \) elements of \( \text{ObjId}_q \).
- \( o' \in N \)
- There is an isomorphism \( \iota \) between the object graph \( g(p(o)) \downarrow_o \) rooted at \( o \) and the object graph \( h' \downarrow_{o'} \) rooted at \( o' \). Further, \( \iota(v) = v \) for \( v \in \text{grObjId} \)
- \( h'_{o'} \subseteq N \cup \text{grObjId} \).
\[ h' = h \cdot [o' \mapsto r] \] where \( r \) is the root object of the graph \( h' \).

We extend this definition to arbitrary values, that is \( \text{copy}(v, q, g) \) is defined to be \( v \) unless \( v \) is an object id, in which case it is defined as above.

**Proposition 2.6.** Let \( g \) is place-local heap. Let \( p, q \in \text{dom}(g) \) be two (not necessarily distinct) places, and let \( o \in \text{ObjId}_p \). Let \( \text{copy}(o, q, g) = (o', g') \). Then \( g' \) is place-local.

Place-shift takes a step to activate. Moreover, in the conclusion of the rule (PLACE SHIFT) the target statement contains a final \( \text{skip} \) in order to model the fact that the remote control has to come back at the local place after executing the remote code \( s[v'/v'] \). This additional step is actually needed in the resilient calculus, where we need to model the case where the remote place precisely fails after executing \( s \) but before the control has come back. Indeed, consider \{\text{at}(p) \{\text{async} s \text{ skip} \} t \} and \{\text{at}(p) \{\text{async} s \} t \}. The local code \( t \) is already active only in the second statement while in the first one it is waiting for the termination of the synchronous remote statement. Accordingly, the second statement models the situation where the control has come back locally after installing the remote asynchronous computation.

As for error propagation, by rule (AT) we have that any exception, either synchronous or asynchronous, that occurred remotely at place \( p \) is homomorphically reported locally at place \( r \). As an example, consider \{\text{at}(p) \{\text{async} s \text{ skip} \} t \} and \{\text{at}(p) \{\text{async} s \} t \}. The local code \( t \) is already active only in the second statement while in the first one it is waiting for the termination of the synchronous remote code. In order to recover from remote exceptions, we can use the try-catch mechanism and write \{\text{at}(r) \{\text{try} (\text{at}(p) \text{ throw E} \) catch t' \} t \} so that the synchronous exception is caught at \( r \) according to the rule (TRY). More precisely, the \( \text{try} \) \( \text{catch} \) \( t \) statement immediately activates \( s \). Moreover, the rule (TRY) shows that asynchronous exceptions are passed through, since they are only caught by \text{finish}. On the other hand, synchronous exceptions are absorbed into a correct transition and the \text{catch}-clause is activated, together with the (asynchronous) statements \( s' \) left behind by the failed \( s \).

2.2 Mechanization in Coq

We have encoded the syntax and semantics of TX10 in Coq, an interactive theorem prover. Encoding the syntax and semantics are mostly straightforward, and closely follows the paper presentation. However, the mechanized formalism has a richer notion of exception propagation, which was omitted from the paper for compactness. Labels can carry a list of exceptions, allowing multiple exceptions to be propagated by Finish (instead of using a single generic exception). Additionally, labels / exceptions can be any value type. This complicates the rules, since the (AT) rule needs to copy any values stored in the labels from the target heap to the caller’s heap. This is done by the actual X10 language, and correctly modeled by our mechanized semantics.

The most challenging part of encoding the semantics is encoding the copy operation given in Definition 2.5 which copies an object graph from one heap to another.
Mechanizing the Copy Operation

Definition 2.5 provides a declarative specification of the copy operation, asserting the existence of a satisfying function. The mechanization explicitly constructs this function. In particular, it provides a pure (provably terminating and side-effect free) function with the given specification.

We first encode definitions of (local) reachability and graph isomorphism, proving key theorems relating them. We also define what it means for a value to be well-formed in a given heap: all objects (locally) reachable from that value must be in the heap. In other words, the object graph rooted at the value may not contain dangling pointers.

The implementation of the copy function itself proceeds recursively. The recursive core of copy is given a list of existing mappings (initially empty) from the source heap to the target heap, the source and target heaps, and the initial object to copy. For each field in the object, if the value is an object identifier, it looks up the identifier in the heap. If heap does not contain the identifier (which means that the given root is not well-formed), the copy operation fails. Otherwise, it creates a new object in the destination heap, and adds a mapping from the the source oid to the new oid. It then calls itself recursively (with the enriched set of mappings) to copy the object into the destination heap. Finally, the destination heap is updated so thenewly created oid contains the copied object returned by the recursive call. The enriched set of mappings is then returned so that it can be reused for the next field in the object.

The tricky part of implementing this algorithm in Coq is proving termination. This is not obvious, since there can be cycles in the object graph that we are copying. To prevent looping on such cycles, the implementation carefully maintains and uses the set of existing mappings from the source to the destination heap. To prove termination for a non-structurally recursive function, we define a well founded measure that provably decreases on every recursive call. We define this measure over the pair of the number of oids in the source heap that are not in the domain of the mappings and the number of fields left in the object. Since the source heap is finite and does not change, this is a well founded relation as long as as either the number of remaining elements goes down (meaning that the number of distinct mappings increases) or it stays the same and the number of fields decreases.

There are two recursive calls in the implementation. The first recursive call is during the processing of a field. If the field contains an oid, then the implementation adds a new pair to the set of mappings before it calls itself. The second recursive calls is part of the iteration over the fields. After processing a single field, it calls itself recursively with the rest of them (without removing any of the accumulated mappings). In both cases, one of the measured metrics decreases, ensuring that the recursive calls terminate.

As well as proving that the implementation is total, we also prove that is has the required specification. Moreover, if copy fails, there must exist some oid reachable from the root which is not contained in the heap. This last part of the specification in turn enables us to prove that copy will always succeed if the initial value is well formed.

2.3 Properties of the transition relation

TX10 satisfies a number of useful properties, given below. We have mechanized these proofs in Coq, using our encoding of TX10. This provides a high level of assurance in
these proofs, and fills in the details of the various well-formedness conditions needed to ensure that the properties hold.

**Proposition 2.7 (Absence of stuck states).** If a configuration \( k \) is terminal then \( k \) is of the form \( g \).

The mechanized proof of this proposition additionally proves that the evaluation relation is computable: if the configuration is not terminal, we can always compute a next step. This is of course not the only step, since the relation is non-deterministic. Similarly, we prove that the transitive closure of the evaluation relation does not get stuck and is computable. This proof can be "run", yielding a simple interpreter for TX10.

**Definition 2.8 (Place-local Configuration).** Given a place-local heap \( g \), we say that a configuration \( \langle s, g \rangle \) is place-local if

- for any local object id \( o \) occurring in \( s \) under \( at(p) \) or \( \overline{at}(p) \), we have that \( o \in \text{dom}(g(p)) \) (hence \( o \in \text{ObjId}_p \) by place-locality of \( g \)), and
- for any global reference \( o \$ q \) occurring in \( s \), we have that \( o \in \text{dom}(g(q)) \).

**Proposition 2.9 (Place-locality).** If \( \langle s, g \rangle \) is a place-local configuration and \( \langle s, g \rangle \xrightarrow{\lambda} \langle s', g' \rangle \) \( \mid g' \), then \( \langle s', g' \rangle \) is a place-local configuration, resp. \( g' \) is a place-local heap.

The following propositions deal with error propagation, whose rationale can be summarized as follows: **synchronous failures** arise from synchronous statements, and lead to the failure of any synchronous continuation, while leaving (possibly remote) asynchronous activities that are running in parallel free to correctly terminate (cf. Proposition 2.10). On the other hand, **asynchronous failures** arise when an exception is raised in a parallel thread. In this case the exception is confined within that thread, and it is caught by the closest \( \text{finish} \) construct that is waiting for the termination of this thread. On termination of all spawned activities, since one (or more) asynchronous exception were caught, the \( \text{finish} \) constructs re-throws a synchronous failure (cf. Proposition 2.11). We rely on the following definition of **Evaluation Contexts**, that is contexts under which a reduction step is possible:

\[
E ::= \emptyset \mid \{ E \, t \} \mid \{ \overline{at}(p) E \} \mid \text{Async} \, E \mid \text{finish}_\mu \, E \mid \text{try} \, E \, \text{catch} \, t
\]

**Proposition 2.10 (Synchronous Failures).** If \( \langle s, g \rangle \xrightarrow{\iota} k \) then \( \vdash \text{isSync} \, s \). Moreover, if \( k \equiv \langle s', g' \rangle \), then \( \vdash \text{Async} \, s' \)

**Proposition 2.11 (Asynchronous Failures).**

- If \( \langle s, g \rangle \xrightarrow{\iota} k \) then there exists an evaluation context \( E[\cdot] \) such that \( s = E[s_1] \) with \( \langle s', g \rangle \xrightarrow{\iota} k' \) and \( \vdash \text{Async} \, s_1 \).
- If \( \langle \text{finish}_\mu, s, g \rangle \xrightarrow{\lambda_1} \ldots \xrightarrow{\lambda_n} g \) because of \( \langle s, g \rangle \xrightarrow{\lambda_1} \ldots \xrightarrow{\lambda_n} g \), then
  1. \( \lambda_i = \epsilon \) for \( i = 1, \ldots, n - 1 \), and
  2. and \( \lambda_n = \epsilon \) if \( \forall j = 1, \ldots, n \ \lambda_j^* = \epsilon \) otherwise \( \lambda_n = E\iota \).

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The proofs of the propositions above easily follow by induction on the derivation of \( \langle s, g \rangle \xrightarrow{\Sigma_p} k \), resp. \( \langle s, g \rangle \xrightarrow{\times_p} k \), and an inspection of the rules for finish.

**Proposition 2.12.** Let be \( \langle s, g \rangle \xrightarrow{\lambda_p} \langle s', g' \rangle \), then if isAsync \( s \) then isAsync \( s' \), or equivalently, if isSync \( s' \) then isSync \( s \)

### 3 Equivalence and Equational Laws

In this section we define a notion of equivalence for TX10 programs along the lines of [21]. We consider weak bisimulation defined on both normal transitions and transitions that throw an exception. Moreover, the bisimulation encodes the observation power of the concurrent context in two ways: (i) it preserves the isSync/isAsync predicate and (ii) takes into account concurrent modification of shared memory. As a result, we have that the resulting equivalence is a congruence (cf. Theorem 3.3).

We use a notion of environment move to model update of shared heap by a concurrent activity. The store can be updated by updating a field of an existing object, by creating a new (local) object, or by means of a serialization triggered by a place shift.

**Definition 3.1 (Environment move).** An environment move \( \Phi \) is a map on global heaps satisfying:

1. If \( g \) is place-local, then \( \Phi(g) \) is place-local,
2. \( \text{dom}(\Phi(g)) = \text{dom}(g) \), and \( \forall p \in \text{dom}(g) \text{ dom}(g(p)) \subseteq \text{dom}(\Phi(g)(p)) \).

Let \( (\longrightarrow_p)^* \) denote the reflexive and transitive closure of \( \longrightarrow_p \), that is any number (possibly zero) of \( \epsilon \)-steps. Then we let \( \xrightarrow{\lambda_p} \) stand for \( (\longrightarrow_p)^* \) when \( \lambda \neq \epsilon \), and \( (\longrightarrow_p)^* \) if \( \lambda = \epsilon \).

**Definition 3.2 (Weak Bisimulation).** A binary relation \( R \) on closed configurations is a weak bisimulation if whenever

1. \( g R k \) then \( k = g \),
2. \( \langle s, g \rangle R k \) then \( k = \langle t, g' \rangle \) for some \( t \), and
   - \( \vdash \) isSync \( s \) if and only if \( \vdash \) isSync \( t \) and
   - for every environment move \( \Phi \), and for every place \( p \) it is the case that
     (a) if \( \langle s, \Phi(g) \rangle \xrightarrow{\lambda_p} \langle s', g' \rangle \) then for some \( t', \langle t, \Phi(g) \rangle \xrightarrow{\lambda_p} \langle t', g' \rangle \) and \( \langle s', g' \rangle R \langle t', g' \rangle \), and vice versa.
     (b) if \( \langle s, \Phi(g) \rangle \xrightarrow{\lambda_p} p \) then \( \langle t, \Phi(g) \rangle \xrightarrow{\lambda_p} p \) and \( g' \) and vice versa.

Two configurations are weak bisimilar, written \( \langle s, g \rangle \equiv \langle t, g' \rangle \), whenever there exists a weak bisimulation relating them. The weak bisimilarity is the largest weak bisimulation between configurations.

**Theorem 3.3.** Weak bisimilarity is a congruence.
We illustrate the equivalence by means of a number of equational laws dealing with
the main constructs of TX10.

\[ \vdash \text{isSync } s \quad \{ \text{skip} ; s \} \equiv s \]  \quad (1)

\[ \vdash \text{isSync } s \quad \{ s \text{skip} ; \} \equiv s \]  \quad (2)

\[ \{ \text{throwv } s \} \equiv \text{throwv} \]  \quad (3)

\[ \{(s) u \} \equiv \{ s \{ t u \} \} \]  \quad (4)

To prove (1) it is sufficient to show that the relation
\[ \{(\langle \{ \text{skip} \ s \} , g \rangle , \langle s , g \rangle ) | \vdash \text{isSync } s \} \cup \text{Id} \] where \text{Id} is the identity relation over configurations, is a weak bisimulation. Observe that (1) and (2) only hold for synchronous statements since both \{ \text{skip } s \} and \{ s \text{skip} \} are synchronous statements irrespective of \( s \), hence the equivalence only holds when also the r.h.s. is synchronous.

\[ \text{tryskipcatch } t \equiv \text{skip} \]  \quad (5)

\[ \vdash \text{isSync } s \quad \text{trythrowvcatch } s \equiv s \]  \quad (6)

\[ \text{tryscatchthrowv } \equiv s \]  \quad (7)

\[ \vdash \text{isAsync } \{ s \} \quad \text{try} \{ s \} \text{catch } u \equiv \{ \text{trycatch } u \text{trycatch } u \} \]  \quad (8)

\[ \text{try} \{ \text{tryscatcht } \text{catch } u \} \equiv \text{try} \text{catch} \text{try} \text{catch } u \]  \quad (9)

Notice that law (8) is not valid, since the execution of the r.h.s. might activate two copies of \( u \) when both \( s \) and \( t \) fail in sequence. On the other hand in the l.h.s. a synchronous error in \( s \) implies that the continuation \( t \) is discarded. Formally, when \( \langle s, g \rangle \overset{\text{skip}}{\rightarrow}_p g' \) then \( \langle \text{try} \{ s \} \text{catch } u, g \rangle \overset{\text{trycatch } u}{\rightarrow}_p \langle u, g' \rangle \) while the r.h.s. reduces to \( \langle \{ u \text{trycatch } u \}, g' \rangle \).

\[ \text{at} (p) \text{skip } \equiv \text{skip} \]  \quad (11)

\[ \text{at} (p) \text{throwv } \equiv \text{throwv} \]  \quad (12)

\[ \text{at} (p) \{ s \} \equiv \{ \text{at} (p) \text{s at} (p) t \} \]  \quad (13)

\[ \text{at} (p) \langle \text{try} \text{catch } t \rangle \text{catch } u \equiv \text{try} \langle \text{at} (p) \text{s catch} \langle \text{at} (p) t \rangle \text{catch} \langle \text{at} (p) t \rangle \rangle \text{at} (q) \text{s } \equiv \text{at} (q) \text{s} \]  \quad (14)

All the laws above for place shift also hold for the dynamic version of \text{at}.

\[ \text{async} \text{skip } \neq \text{skip} \]  \quad (16)

\[ \text{asyncthrowv } \neq \text{throwv} \]  \quad (17)

\[ \vdash \text{isAsync } s \quad \{ \text{asyncthrowv } s \} \equiv \{ s \text{asyncthrowv} \} \]  \quad (18)

\[ \text{async at} (p) s \equiv \text{at} (p) \text{async } s \]  \quad (19)

\[ \text{asyncasync } s \equiv \text{async } s \]  \quad (20)

\[ \vdash \text{isAsync } s, \text{isAsync } t \quad \{ s t \} \equiv \{ t s \} \]  \quad (21)

\[ \vdash \text{isAsync } s \quad \text{try} \{ s \} \text{catch } u \equiv \{ s \text{trycatch } u \} \]  \quad (22)

Laws (16) do not hold since only the l.h.s. are asynchronous. Law (17) does not hold since weak bisimilarity counts the number of (asynchronous) exceptions, and the l.h.s.
throws two asynchronous $E \times$ while the r.h.s. just one. Notice that by law (3) we have
\{throw $v$ throw $v$\} $\equiv$ throw $v$, which is correct since the l.h.s. throws a single $E \otimes$
since synchronous errors discard the continuation.

Observe that the static version of law (18) does not hold, i.e., $\{\text{async throw } v\ s\} \neq
\{s \text{ async throw } v\}$ since only in the r.h.s. the statement $s$ can make a move. On the
other hand, the dynamic version of laws (19) and (20) are valid. Law (21) comes observing that the relation \{((\{s \ t\}, g), (\{t \ s\}, g)) | \vdash \text{isAsync } s, \text{isAsync } t\} $\cup$ $Id_{k}$ is a
weak bisimulation. Finally observe that law (22) only holds for asynchronous $s$ since a
synchronous error thrown by $s$ would be caught in the l.h.s. while in the r.h.s. it would
discard the continuation.

\[
\begin{align*}
\text{finish skip} & \equiv \text{skip} \quad (23) \\
\text{finish throw } v & \not\equiv \text{throw } v \quad (24) \\
\text{finish } \{s \ t\} & \equiv \text{finish } s \text{ finish } t \quad (25) \\
\text{finish } \{s \text{ throw } v\} & \not\equiv \{\text{finish } s \text{ throw } v\} \quad (26) \\
\text{finish async } s & \equiv \text{finish } s \quad (27) \\
\text{finish } \{s \text{ async } t\} & \equiv \text{finish } \{s \ t\} \quad (28)
\end{align*}
\]

Law (24) does not hold because of the exception masking mechanism. More precisely,
the exception $v \otimes$ thrown by $\text{throw } v$ is masked in the l.h.s. by $E \otimes$ by the finish
construct. For the same reason also law (26) does not hold. Law (28) comes form (25) and
(27). In the following final set of laws we write $\vdash \text{noAsync } s$ if $s$ has no sub-term of the
form async $s'$ for some $s'$, i.e., if $s$ cannot evolve to an asynchronous statement.

\[
\begin{align*}
\text{finish at } (p) s & \equiv \text{at } (p) \text{ finish } s \quad (29) \\
\text{finish } \{\text{async throw } v\ s\} & \equiv \{\text{finish } s \text{ throw } v\} \quad (30) \\
\text{finish finish } s & \equiv \text{finish } s \quad (31) \\
(\vdash \text{noAsync } s) \text{ finish } s & \not\equiv s \quad (32) \\
(\vdash \text{noAsync } s) \text{ finish } \{s \ t\} & \not\equiv \{s \text{ finish } t\} \quad (33) \\
(\vdash \text{noAsync } s) \text{ finish try } s \text{ catch } t & \not\equiv \text{try } s \text{ catch } \text{finish } t \quad (34)
\end{align*}
\]

Again law (32), and then also (33) and (34), does not hold because of the exception
masking mechanism performed by the finish construct.

## 4 Resilient TX10

The resilient calculus has the same syntax of TX10. We now assume that any place
$p \in P \setminus \{0\}$ can fail in any moment during the program computation. Place 0 has a
special role: programs start at place zero, then this place is used to communicate the
result to the user, so we assume it can never fail (if it does fail, the whole execution is
torn down). In order to define the semantics, we now let global heaps $g$ to be partial
(rather than total) maps from places to local heaps. Intuitively, $\text{dom}(g)$ is the set of
non failed places. The semantics of Resilient TX10 is given by the rules in Table 3 and
Table 4 from Section 2 plus the rules in Tables 6, 7 and 8 given in this section. More
precisely, the resilient calculus inherits form TX10 the rules for expression evaluation
(Place Failure)  
\[ p \in \text{dom}(g) \]  
\[ \langle s, g \rangle \xrightarrow{p} \langle s, g \setminus \{(p, g(p))\} \rangle \]

(Spawn)  
\[ p \in \text{dom}(g) \]  
\[ \langle \text{async } s, g \rangle \xrightarrow{p} \langle \text{async } s, g \rangle \]
\[ p \notin \text{dom}(g) \]  
\[ \langle \text{async } s, g \rangle \xrightarrow{\text{DP} \otimes} p \]

(Local Failure)  
\[ p \notin \text{dom}(g) \]  
\[ \langle \text{skip}, g \rangle \xrightarrow{\text{DP} \otimes} p \]
\[ \langle \text{throw } v, g \rangle \xrightarrow{\text{DP} \otimes} p \]
\[ \langle \text{val } x = e \cdot s, g \rangle \xrightarrow{\text{DP} \otimes} p \]
\[ \langle e.f = e_2, g \rangle \xrightarrow{\text{DP} \otimes} p \]

(Async)  
\[ \lambda = \epsilon \]  
\[ \langle \text{async } s, g \rangle \xrightarrow{p} \langle \text{async } s', g' \rangle \mid g' \]
\[ \lambda = v \times \]  
\[ \langle \text{async } s, g \rangle \xrightarrow{\text{Msk}(v \times)} p \langle \text{async } s', g' \rangle \mid g' \]

(Finish)  
\[ \langle s, g \rangle \xrightarrow{p} \langle s', g' \rangle \]
\[ \langle \text{finish}_\mu s, g \rangle \xrightarrow{p} \langle \text{finish}_\mu \cup \lambda s', g' \rangle \]

(End of Finish)  
\[ \langle s, g \rangle \xrightarrow{p} \langle s', g' \rangle \]
\[ \lambda' = \begin{cases} 
\epsilon & \text{if } \lambda \cup \mu = \emptyset \\
\text{E} \otimes & \text{if } \lambda \cup \mu \neq \emptyset, p \in \text{dom}(g) \\
\text{DP} \otimes & \text{if } \lambda \cup \mu \neq \emptyset, p \notin \text{dom}(g) 
\end{cases} \]
\[ \langle \text{finish}_\mu s, g \rangle \xrightarrow{\text{Msk}(\lambda') \otimes} p \]

Table 6. Resilient Semantics I

(i.e., Table 3 and those in Table 4 which correspond to basic statement executed at non-failed place \( p \), i.e. \( p \in \text{dom}(g) \). The rules for TX10’s main constructs, i.e. those in Table 5 hold also in the resilient calculus when \( p \in \text{dom}(g) \), but they must be integrated with additional rules dealing with the case where the local place \( p \) has failed. Therefore, in order to improve the presentation, rather than inheriting Table 5, we collect here all the operational rules for the main constructs, compacting them in Tables 6, 7 and 8.

The place failure may occur at anytime, and it is modelled by the rule (Place Failure) which removes the failed place from the global heap. The semantics of TX10 is then extended so to ensure that after the failure of a place \( p \):

1. any attempt to execute a statement at \( p \) results in a DP exception (Proposition 4.6);
2. place shifts cannot be initiated form \( p \) nor launched to the failed \( p \) (rule (Place Shift));
3. any remote code that has been launched from \( p \) before its failure is not affected and it is free to correctly terminate its remote computation. If a synchronous exception escapes from this remote code and flows back at the failed place, then this exception is masked by a DP (Proposition 4.7) which is thrown back to a parent finish construct waiting at a non failed place.

More precisely, we will show that the operational semantics of Resilient TX10 enforces the following three design principles:

1. **Happens Before Invariance Principle**: failure of a place \( q \) should not alter the happens before relationship between statement instances at places other than \( q \).
2. **Exception Masking Principle**: failure of a place \( q \) will cause asynchronous exceptions thrown by \( \alpha \) \( (q) \) \( s \) statements to be masked by DP exceptions.

3. **Failed Place Principle**: at a failed place, activating any statement or evaluating any expression should result in a DP exception.

We now precisely illustrate the rules for the main constructs. The rule (LOCAL FAILURE) shows that no expression is evaluated at a failed place and any attempt to execute a basic statement at the failed place results in a synchronous DP exception. Similarly, rule (SPAWN) shows that new activities can only be spawned at non-failed places. On the other hand, rule (ASYNC) is independent from the failure of \( p \), so that any remote computation contained in \( s \) proceeds not affected by the local failure. The semantics of `finish` is the same as in Section 2 but for the rule (END OF FINISH), which now ensures that when \( p \notin \text{dom}(g) \) a DP\( \otimes \) (rather than E\( \otimes \)) exception is thrown whenever one of the governing activities (either local or remote) threw an exception.

The rules for sequences are collected in Table 7. Rules (SEQ) and (PAR) are the same as in the basic calculus, allowing remote computation under sequential or parallel composition to evolve irrespective of local place failure. The failure of \( p \) plays a role only in rule (SEQ FAILED TERM): in this case the termination of the first component \( s \) in the sequence \( \{s t\} \) always results in a DP exception. Moreover, the continuation \( t \) is discarded when \( s \) is a synchronous statement. On the other hand, when \( s \) is an asynchronous statement, \( t \) might be an already active remote statement, hence the rule gives to \( t \) the chance to correctly terminate.

Rule (PLACE SHIFT) allows the activation of a place-shift only when both the source and the target of the migration are non-failed places. Rule (AT) behaves like in TX10 except that it masks any remote synchronous exception with a DeadPlaceException. As an example consider \( \alpha (p) \{\alpha (q) s \} \alpha (r) t \): if \( p \) fails while \( s \) and \( t \) are (remotely) executing, it is important not to terminate the program upon completion of just \( s \) (or just \( t \)). Then with rule (AT) we have that a remote computation silently ends even if the control comes back at a failed home. As another example, consider...
waiting at non failed place

discarded. Notice that enclosing the inner place, termination and error detection in
useful when an exception that should be detected by the inner
we have that the
executed at
failed place
the other hand, we can recover from an exception in
clause is never executed, hence he two programs above have the same semantics. On
assume that both
Example 4.1. Let also assume that

\[ \lambda = \epsilon, v \times (\text{try } s \text{ catch } t, g) \xrightarrow{\lambda} p (\text{try } s' \text{ catch } t, g') | g' \]

\[ p \in \text{dom}(g), \lambda = v \otimes (\text{try } s \text{ catch } t, g) \xrightarrow{\lambda} p ([s't], g') | (t, g') \]

\[ p \notin \text{dom}(g), \lambda = D \otimes (\text{try } s \text{ catch } t, g) \xrightarrow{\lambda} p (s', g') | g' \]

**Table 8. Resilient Semantics III**

\[ \overline{\text{at}}(r) \{ \overline{\text{at}}(p) \text{skip} \ t \} \text{ with } p \notin \text{dom}(g), \text{ then the failure of skip at } p \text{ must be}
\]

reported at r as a synchronous error so that the continuation t is discarded.

**Example 4.1.** Consider the following program, where the code \( s_q \) is expected to be
executed at \( g \) after the termination of any remote activities recursively spawned at \( p \):

\[ \overline{\text{at}}(q) \{ \text{finish async} \overline{\text{at}}(p) \{ \text{finish } s \ s_p \} \ s_q \} \]

Let also assume that \( s \) spawns new remote activities running in a third place \( r \). Now, assume that both \( p \) and \( r \) fail while \( s \) is (remotely) executing. We have that \( s \) throws an exception that should be detected by the inner \text{finish}, however since \( p \) is a failed place, termination and error detection in \( s \) must be delegated to the outer \text{finish}
waiting at non failed place \( q \); that is indeed performed by rule (END OF FINISH). Hence we have that the \text{finish at } q \text{ throws a synchronous error and the continuation } s_q \text{ is}
discarded. Notice that enclosing the inner \text{finish} within a try-catch construct is only useful when \( p \) is a non failed place. Indeed, consider the program

\[ \overline{\text{at}}(q) \{ \text{finish async} \overline{\text{at}}(p) \{ \text{try} (\text{finish } s) \text{ catch } t \ s_p \} \ s_q \} \]

then by the rule (TRY) for exception handling we have that when \( p \) is a failed place the clause is never executed, hence he two programs above have the same semantics. On the other hand, we can recover from an exception in \( s \) by installing a try/catch at the non failed place \( q \): \( \overline{\text{at}}(q) \{ \text{try} (\text{finish async} \overline{\text{at}}(p) \{ \text{finish } s \ s_p \}) \text{ catch } t \ s_q \} \).
4.1 Properties of the transition relation

The main properties of the operational semantics of TX10 scale to Resilient TX10. We have encoded the syntax and semantics of Resilient X10 in Coq, as we did for TX10 (see Section 2.2). Using this encoding, we have mechanized the analogous proofs for Resilient X10.

Proposition 4.2 (Absence of stuck states). If a configuration $k$ is terminal then $k$ is of the form $g$.

The definition of place-locality of configurations must be generalized to the case of partially defined heaps. More precisely, given a configuration $\langle s, g \rangle$, any local oid $o$ is $s$ must be locally defined, while a global reference $o \$ p$ might now be a dangling reference since the global object’s home place $p$ might have failed.

Definition 4.3 (Place-local Resilient Configuration). Given a place-local heap $g$, we say that a configuration $\langle s, g \rangle$ is place-local if

$\forall p \in \text{dom}(g)$ for any local object id $o$ occurring in $s$ under $at(p)$ or $\overline{at}(p)$, we have that $o \in \text{dom}(g(p))$ (hence $o \in \text{ObjId}_p$ by place-locality of $g$).

Given the definition above, we can still prove that resilient semantics preserves place-locality of resilient configurations.

Proposition 4.4 (Place-locality). If $\langle s, g \rangle$ is a place-local resilient configuration and $\langle s, g \rangle \xrightarrow{\lambda} p \langle s', g' \rangle | g'$, then $\langle s', g' \rangle$ is a place-local resilient configuration, resp. $g'$ is a place-local heap.

Also Proposition 2.10 and 2.11 hold also in Resilient TX10, with a minor modification: in the second clause of Proposition 2.11 the final error thrown by a finish construct might be either $E \otimes$ or $\text{DP} \otimes$.

The main results of this section are the three principles stated above. The Exception Masking Principle, formalized by Theorem 4.5, shows that no exception other than $\text{DP}$ can arise from a failed place. The Failed Place Principle, formalized by Theorem 4.8, shows that no statement can be executed at a failed place. Finally, the Happens Before Invariance Principle shows in Theorem 4.10 that the place failures do not alter the happens before relation between the non-failed statements.

Theorem 4.5 (Exception Masking Principle). Let be $p / \in \text{dom}(g)$ and $\langle s, g \rangle \xrightarrow{\lambda} p k$. If $\lambda = v \otimes$, then $v = \text{DP}$.

Let say $\vdash \text{isLocal } s$ whenever $s$ does not contain active remote computation, that is $s$ has no substatements of the form $\text{at}(q) s'$. We say $\vdash \text{isRemote}_p s$ when any basic statement in $s$ occurs under a $\overline{at}(q)$ construct for some place $q$ with $q \neq p$.

Proposition 4.6 (Local failure). Let be $p / \in \text{dom}(g)$ and $\langle s, g \rangle \xrightarrow{\lambda} p k$.

- If $\vdash \text{noAsync } s$ and $\vdash \text{isLocal } s$, then $\lambda = \text{DP} \otimes$ and $k = g$.
- If $\vdash \text{isLocal } s$, then either
• $\lambda = \text{DP} \otimes \text{or } \lambda = \text{DP} \times \text{or }$

$s = E[\text{finish}_t]\{s, g\} \rightarrow_p \langle s', g' \rangle \rightarrow_p \langle t', g' \rangle$ with $s' = E[\text{finish}_t]p'$ and $(t, g) \rightarrow_p \langle t', g' \rangle$.

The following proposition states that remote computation at non-failed place proceeds irrespective of local place failure, but for the exception masking effect.

**Proposition 4.7 (Remote computation).** Let $\Rightarrow_p$ isRemote$_p s$. If $\langle s, g \rangle \rightarrow_p \langle s', g' \rangle \mid g'$ with $p \in \text{dom}(g)$, then $\langle s, g \rangle \rightarrow_p \langle s, g \setminus \{(p, g(p))\} \rangle \rightarrow_p \langle s', g' \rangle \mid g'_s$ where $g'_s = g' \setminus \{(p, g'(p))\}$ and $\lambda' = \lambda$ if $\lambda = \text{e, v x}$ while $\lambda' = \text{DP} \otimes \text{if } \lambda = \text{v x}$. Moreover $\Rightarrow_p$ isRemote$_p s'$.

**Theorem 4.8 (Failed Place Principle).** If $s$ performs a correct step at a failed place, i.e., $\langle s, g \rangle \rightarrow_p \langle s', g' \rangle \mid g'$ with $p \notin \text{dom}(g)$, then either

- $s$ contains a substatement that remotely computed a correct step at a non failed place, i.e., $s = E[s_1]$ with $\Rightarrow_p$ isRemote$_p s_1, \langle s_1, g \rangle \rightarrow_p \langle s'_1, g' \rangle \mid g'$ and $s' = E[s'_1]$, or
- a local activity ends at $p$ with a DP that has been absorbed by a governing finish, i.e. $s = E[\text{finish}_t]$, $s' = E[\text{finish}_t]p'$ and $(t, g) \rightarrow_p \langle t', g' \rangle$.

We denote by $\bar{k}$ a trace $\langle s_0, g_0 \rangle \xrightarrow{\lambda_1 \gamma_0} \langle s_1, g_1 \rangle \xrightarrow{\lambda_2 \gamma_0} \cdots \xrightarrow{\lambda_n \gamma_0} \langle s_n, g_n \rangle$. Moreover we write $|\bar{k}|$ for the length $n$ of such a trace, and $k_i$ to indicate the $i$-th configuration $\langle s_i, g_i \rangle$, $i = 0, \ldots, n$. We define below the Happens Before relation in terms of the operational semantics. Intuitively, given a program $s$ with two substatements $s_1, s_2$, we say that $s_1$ happens before $s_2$ whenever in any program execution $s_1$ is activated, i.e. it appears under an evaluation context, before $s_2$. We refer to [24] for a static definition of the happens before relation in terms of static statements, which is also proved to be equivalent to a dynamic characterization that correspond to the following one.

**Definition 4.9 (Happens Before).** Let $s_0$ be a program and let $s_1, s_2$ be two substatements of $s_0$. Then we say that $s_1$ happens before $s_2$, written $s_1 < s_2$, whenever for any trace $\bar{k}$ such that $k_0 = \langle s_0, g_0 \rangle$ and $k_i[\bar{k}] = \langle E[s_2 \rho], g \rangle$ for some $g$, some evaluation context $E$ and some variable substitution $\rho$, there exists $i \in 0, \ldots, |\bar{k}|$ such that $k_i = \langle E'[s_1 \rho'], g' \rangle$ for some $g', E', \rho'$.

Notice that the definition of the Happens Before relation is parametric on a transition relation. Let write $s_1 < s_2$ when we restrict to (traces in) TX10 semantics, and $s_1 < R s_2$ when considering (traces in) the resilient semantics.

**Theorem 4.10 (Happens Before Invariance).** Let $s_0$ be a program and let $s_1, s_2$ be two substatements of $s_0$. Then $s_1 < s_2$ if and only if $s_1 < R s_2$. 
4.2 Equational laws

The equational theory of TX10 can be smoothly generalized to the resilient calculus.
In order to scale the notion of weak bisimilarity to Resilient TX10 we have to consider
generalized environment moves that take into account the failure of a number of places.

**Definition 4.11 (Resilient Environment move).** An environment move $\Phi$ is a map on
global heaps satisfying:

1. if $g$ is place-local, then $\Phi(g)$ is place-local,
2. $\text{dom}(\Phi(g)) \subseteq \text{dom}(g)$, and $\forall p \in \text{dom}(\Phi(g)) \text{ dom}(\Phi(g)(p)) \subseteq \text{dom}(\Phi(g)(p))$.

The weak bisimilarity for Resilient TX10 is then defined as in Definition 3.2, where
we rely on resilient environment moves and the operational steps used in the bisimulation
game are those defined in this section. In particular, this means that also place
failures occurring at any time must be simulated by equivalent configurations. We dis-
cuss in the following which laws are still valid in the Resilient calculus.

\[
\begin{align*}
\vdash & \text{noAsync } s \quad \vdash \text{isLocal } s \quad \{\text{skip;} s\} \equiv s \quad (35) \\
\vdash & \text{isSync } s \quad \{s \text{ skip;}\} \neq s \\
& \quad \{\text{throw } s\} \equiv \text{throw } v \\
& \quad \{\{s\} \ u\} \equiv \{s \{t\} \ u\} \\
\vdash & \text{noAsync } s \quad \vdash \text{isLocal } s \quad \text{try} \text{throw } v \text{ catch } s \equiv \text{try } \text{at } (p) \text{ s } \text{catch } \text{at } (p) t \quad (39)
\end{align*}
\]

In order for law (1) of Section 2 to be valid also at a failed place, law (35) requires a
stronger constraint for $s$ so to ensure that in that case also the r.h.s always throw a DP⊗.
On the other hand law (36) never holds since the failure of the local place can happen
after the completion of $s$ but before the execution of skip, thus only the l.h.s. would
throw a DP⊗. As for the Try/Catch constructs, all the rules of TX10 are still valid, but
for rule (6), which must be substituted by law (39). Indeed, similarly to law (35), we
must ensure that $s$ throws a synchronous DP⊗ error whenever the local place is failed.

\[
\begin{align*}
\text{at } (p) \text{ skip} \neq \text{skip} & \quad \overline{\text{at } (p)} \text{ skip} \neq \text{skip} \quad (40) \\
\text{at } (p) \text{ throw } v \equiv \text{throw } v & \quad \overline{\text{at } (p)} \text{ throw } v \equiv \text{throw } v \\
\text{at } (p) \{s\} \neq \{\text{at } (p) s\} \text{ at } (p) t & \quad (42) \\
\overline{\text{at } (p)} \{s\} \overline{\text{at } (p) t} & \equiv \overline{\text{at } (p)} \{\text{at } (p) s\} \overline{\text{at } (p) t} \\
\text{at } (p) \text{ (try } s \text{ catch } t) \neq \text{try } \text{at } (p) s \text{ catch } \text{at } (p) t & \quad (44) \\
\overline{\text{at } (p)} \text{ at } (q) s \neq \text{at } (q) s & \quad \overline{\text{at } (p)} \overline{\text{at } (q)} s \neq \overline{\text{at } (q)} s \quad (45)
\end{align*}
\]

The laws (40) for place shift does not hold in the resilient calculus since they involve
two terms that run in different places that might fail in different moments. Notice that
law (41) is still valid by means of the exception masking principle. Rule (42) does not
hold anymore since the local place can fail after the completion of $s$ but before the place
shift of $t$. On the other hand law (43) is still valid since both terms already run at the
same place $p$ and the failure of local place does not affect remote computation. Law
(44) does not hold anymore since $p$ may fail after $s$ has thrown an exception but before
the activation of the handling $t$. The first law (45) does not hold since $p$ may fail before
the place-shift at \( q \), while the second law does not hold since the failure of \( p \) would mask any exception thrown at \( q \).

\[
\begin{align*}
\vdash \text{isAsync}\ s &\quad \{ \text{async\ throw\ } v\ s \} \equiv \{ \text{async\ throw\ } v \} \quad (46) \\
\text{async\ at\ } (p)\ s &\not\equiv \text{at\ } (p)\ \text{async\ } s \quad (47) \\
\overline{\text{async\ at\ } (p)\ s} &\not\equiv \overline{\text{at\ } (p)\ \text{async\ } s} \quad (48) \\
\text{async\ async\ } s &\equiv \text{async\ } s \quad (49)
\end{align*}
\]

\[
\begin{align*}
\vdash \text{isAsync}\ s, \text{isAsync}\ t &\quad \{ s, t \} \equiv \{ t, s \} \quad (50) \\
\vdash \text{isAsync}\ s &\quad \text{try\ } \{ s, t \} \text{ catch\ } u \equiv \{ s\ \text{try\ catch\ } u \} \quad (51) \\
\text{finish\ at\ } (p)\ s &\not\equiv \text{at\ } (p)\ \text{finish\ } s \quad (52)
\end{align*}
\]

Laws (47) (48) does not hold anymore because of the exception masking effect. Indeed, if \( s \) remotely throws a synchronous exception \( v\otimes \), we have that the r.h.s. throws a \( v\times \) exception while the l.h.s. throws \( DP\otimes \) by means of masking.

All the laws for finish hold also in Resilient TX10 but for the one involving place shifting. In law (52) a difference appears between the two terms when the remote place \( p \) fails after the remote code has been activated. In this case \( s \) throws a \( DP \) exception at the failed place, but in the l.h.s. the local (non failed) \( finish \) masks this exception as a generic \( E \), while in the r.h.s. the exception reported locally is still \( DP \).

5 Conclusions and Future work

We have studied a formal small-step structural operational semantics for TX10, that is a large fragment of the X10 language covering multiple places, shared mutable objects, sequences, async, finish, at and try\slash catch constructs. We have then shown that this framework smoothly extends to the case where places dynamically fail. Failure is exposed through exceptions thrown by any attempt to execute a statement at the failed place. The error propagation mechanism in Resilient TX10 extends that of TX10 (i) by discarding exception handling at failed places, i.e. no \texttt{catch} clause is ever executed at failed places, and (ii) by masking with a \texttt{DeadPlaceException} any remote exception flowing back at the failed place. Moreover, we established a Happens Before Invariance Principle showing that the failure of a place \( p \) does not alter the happens before relationship between statements at places other than \( p \).

As an example of formal methods that can be developed on top of the given operational semantics, we studied a bisimulation based observation equivalence. We showed that it correctly encodes the observation power of the concurrent context by proving that it is a congruence. We illustrated this equivalence by means of a number of laws dealing with the main constructs of the language, discussing which of these equivalences are invariant under place failures. The axiomatization of the given equivalence is left for future work. We think that the resilient equational theory opens the way to the development of laws that can be used in the X10 compiler to optimize programs, e.g. using polyhedral analysis [24]. We also plan for future work the extension of the framework we presented to cover the \texttt{atomic} and \texttt{when} constructs from X10. We also plan to develop denotational semantics for TX10 based on a pomset model that naturally allows the definition of the happens before relation. Another promising approach
seems to be the study of full abstraction by extending to this setting the trace set model of S. Brookes [7].

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