Directed search for continuous gravitational waves from the Galactic center

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We present the results of a directed search for continuous gravitational waves from unknown, isolated neutron stars in the Galactic center region, performed on two years of data from LIGO’s fifth science run from two LIGO detectors. The search uses a semicoherent approach, analyzing coherently 630 segments, each spanning 11.5 hours, and then incoherently combining the results of the single segments. It covers gravitational wave frequencies in a range from 78 to 496 Hz and a frequency-dependent range of first-order spindown values down to $-7.86 \times 10^{-8}$ Hz/s at the highest frequency. No gravitational waves were detected. The 90% confidence upper limits on the gravitational wave amplitude of sources at the Galactic center are $\sim 3.35 \times 10^{-25}$ for frequencies near 150 Hz. These upper limits are the most constraining to date for a large-parameter-space search for continuous gravitational wave signals.

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I. INTRODUCTION

In the past decade the LIGO Scientific Collaboration and the Virgo Collaboration have developed and implemented search techniques to detect gravitational wave (GW) signals. Among others, searches for continuous gravitational waves (CGWs) from known objects have been performed [1], including, for example, searches for CGWs from the low-mass x-ray binary Scorpius X-1 [2,3], the Cas A central compact object [4] and the Crab and Vela pulsars [5–7]. Extensive all-sky studies searching for as yet unknown neutron stars have been performed in recent years [8–14]. Because of the very weak strength of CGW signals, long integration times—of order weeks to years—are required to detect a signal above the noise. When the parameter space to search is large, this is computationally expensive, and techniques have been developed to maximize the attainable sensitivity at fixed computing cost.

In this paper we present the first directed search for gravitational waves from yet unknown, isolated neutron stars in the direction of the Galactic center. We use the term Galactic center (GC) as a synonym for the coordinates of Sagittarius A* (Sgr A*). Current evolutionary scenarios predict that pulsars are born in supernova explosions of massive stars [15]. At least three stellar clusters in the GC region contain massive stars [16] making the GC a promising target for this search. Due to the high dispersion measure toward the GC, however, out of $\sim 2000$ known pulsars [17] only six are located within $\sim 240$ pc of Sgr A* [18], of which four are within $\sim 24$ to $\sim 36$ pc of Sgr A* [16] and one magnetar is less than 2 pc away from Sgr A* [19]. Twenty pulsar wind nebulae are believed to be within 20 pc from Sgr A* [20]. The existence of these objects supports the belief that the GC might harbor a large population of pulsars [16] not apparent to radio surveys because of the dispersion of the radio signal by galactic matter along the line of sight.

The fact that this search targets previously unknown objects leads to a very large parameter space to be covered. A coherent search, which consists of matched filtering the data against single templates over long observation times and over a large parameter space, would have difficulty reaching an interesting sensitivity with reasonable computational power, so we resort to using a hierarchical search technique [21,22] that allows us to integrate over the entire data set of LIGO’s fifth science run (S5). This consists of a coherent step over shorter duration segments, using a maximum-likelihood statistic [23,24], followed by an incoherent combination of the results from these segments.
The plan of the paper is as follows: We start with the scientific motivation of the search (Sec. II) and illustrate the parameter space and the setup (Sec. III A). Then we present the selection of the used data set (Sec. III B). We briefly describe the analysis method and the computational setup (Sec. III C). The various stages of postprocessing and a coherent follow-up search are presented in Sec. III D. No candidate was confirmed by the follow-up. We set 90% confidence upper limits on the GW amplitude (Sec. IV) and discuss the results in Sec. V.

II. MOTIVATION

Rapidly rotating neutron stars with small deviations from perfect axial symmetry are the most promising sources for continuous gravitational wave emission. No search for gravitational waves from such sources, however, has resulted in a detection yet. A possible explanation is that the detectors were not sensitive enough or that the nearest neutron stars all happen to be very close to axisymmetric. Therefore, the most interesting regions are those that contain a large number of yet undiscovered neutron stars. Among such a large population it might be possible to find one neutron star that has a gravitational wave luminosity high enough or that is unusual enough to be detected with this search.

The GC area is believed to be such a region. The central parsec is one of the most active massive star formation regions and is believed to contain about 200 young massive stars [25,26]. Because of this overabundance of massive stars, it is assumed to contain also a large number of neutron stars [18]. Massive stars are believed to be the progenitors of neutron stars: the star undergoes a supernova explosion and leaves behind the neutron star. The wide GC area (R ≤ 200 pc) contains more stars with initial masses above 100 M⊙ than anywhere else known in the Galaxy, plus three of the most massive young star clusters [27]. One of these is the central cluster, which is concentrated around the center of the Galaxy and contains at least 80 massive stars [27]. In the innermost 1 pc, the main electromagnetic radiation comes from only a few supergiants [28], which are located in a dense, rich cluster, centered around Sgr A*. Among the brightest stars we find 20 hot, massive supergiants. These stars form a subgroup concentrated strongly towards the center. The core radius of the entire central cluster is about 0.38 pc [29]. The formation of so many massive stars in the central parsec remains a mystery [27], but current estimates predict roughly as many pulsars within 0.02 pc distance to Sgr A* as there are massive stars [30]. Current estimates assume at least ∼100 radio pulsars to be presently orbiting Sgr A* within this distance [30].

III. THE SEARCH

A. The parameter space

The targets of this search are GWs from fast-spinning neutron stars with a small deviation from perfect axial symmetry. If the star rotates about its principal moment of inertia axis Izz, the equatorial ellipticity ϵ of the neutron star is defined to be the fractional difference in the other moments of inertia,

\[ \epsilon = \frac{I_{xx} - I_{yy}}{I_{zz}}. \]  

The amplitude of a CGW from a source emitting due to an ellipticity ϵ from a distance r is [23]

\[ h_0 = \frac{4\pi^2 G I_{zz} f^2}{c^4 r} \epsilon, \]  

where G is the gravitational constant, c is the speed of light, and the gravitational wave frequency is twice the star’s rotational frequency, f = 2ν.

The range of frequencies that is covered by this search spans 78 to 496 Hz and is located around the most sensitive region of the detectors (around 150 Hz). Based on the computational feasibility of the search, the first-order spindown spans − f/200 yr ≤ ˙f ≤ 0 Hz/s. These ranges of frequencies and spindowns have to be covered with a set of discrete templates. The coherent analysis of the single data segments is done on a coarse rectangular grid in frequency and spindown. At the combination step the spindown parameter is refined by a factor γ of O(1000).

The resolutions are

\[ df = T_{\text{seg}}^{-1}, \quad d\dot{f}_{\text{coarse}} = T_{\text{seg}}^{-2}, \quad d\dot{f}_{\text{fine}} = \gamma^{-1} T_{\text{seg}}^{-2}. \]

with γ = 3225. This choice leads to an average mismatch\(^1\) of ∼0.15. In only a small fraction of cases (1%), the mismatch could be as high as 0.4.

The search assumes a GW source at the position of the dynamical center of the Galaxy, the ultracompact source Sgr A* [31],

\[ \alpha = 4.650 \text{ rad} \quad \text{and} \quad \delta = -0.506 \text{ rad}. \]

The angular resolution is such that the initial search is sensitive to sources within a distance R ≤ 8 pc around Sgr A*, although a coherent follow-up stage (Sec. III D) focuses on the region with R ≤ 3 pc.

B. The data

The data used for the search come from two of the three initial LIGO (Laser Interferometer Gravitational-Wave Observatory) detectors. Initial LIGO consists of two 4-km-arm instruments in Livingston, Louisiana (L1) and Hanford, Washington (H1) and a 2-km-long detector colocated in Hanford (H2). For this search we use data from H1 and L1 at the time of the fifth science run [32]. The fifth science run, called S5, started on November 4, 2005, at 16:00 UTC in Hanford and on November 14, 2005, at

\(^1\)The fractional loss in detection statistic due to the finite resolution in template parameters is called mismatch.
16:00 UTC in Livingston and ended on October 1, 2007, at 00:00 UTC.

There exist a number of reasons for interruption of the data collection process: the detectors experience unpredictable loss of lock from seismic disturbances (earthquakes or large storms), as well as anthropogenic activities. In addition to these down-times, scheduled maintenance breaks and commissioning take place. Some data are excluded from the analysis because of poor data quality. The remaining data are calibrated to produce a gravitational wave strain $h(t)$ time series \[12,32\]. The time series is then broken into 1800-s-long segments. Each segment is high-pass filtered above 40 Hz, Tukey windowed, and Fourier transformed to form short Fourier transforms (SFTs) of $h(t)$. These SFTs form the input data to our search code.

During S5 the detectors were operating close to or at their design sensitivity. The average strain noise of H1 and L1 was below $2.5 \times 10^{-23}$ Hz$^{-1/2}$ in the most sensitive frequency region (around 150 Hz). The performance of the detectors as well as the duty cycle improved over the course of the S5 run.

Our data comprise 630 segments, each spanning 11.5 hours of coincident data in H1 and L1 with the best sensitivity to a CGW signal from the GC. This setup yields the best sensitivity for given computational resources. To select the 630 segments, we use a running window of the size 11.5 h, calculate the expected signal-to-noise ratio (SNR) assuming a constant strength of the GW signal coming from the GC for the particular segment, and move the window by half an hour. To optimize sensitivity, we sort the so-obtained list of segments by their SNR values, pick the best segment, remove from the list all segments that overlap this segment and then select the next segment by taking the next on the list. This procedure is repeated until the 630th segment.

C. The analysis method

We use the hierarchical approach of \[33\] (known as the global correlation transform) and divide the data into single segments, which are coherently analyzed and afterwards incoherently combined. We use the search algorithm HIERARCHSEARCHGCT that is part of the LAL/LALAPPS software suite \[34\]. The coherent analysis of each single data segment is done with a matched filter technique called the $\mathcal{F}$ statistic \[23,24\], which has been used extensively in CGW searches, most recently in \[4,14\]. The incoherent combination step is simply a sum. What to sum, i.e., the mapping between the coarse grid and the fine grid, is described in the references provided on the global correlation transform \[22,33\].

The gravitational wave amplitude $h(t)$ at the output of each detector is a linear combination of the gravitational wave functions $h_+\,$ and $h_\times\,$, where $+$ and $\times$ denote the two different polarizations of the gravitational wave signal

\[ h(t) = F_+(t)h_+(t) + F_\times(t)h_\times(t). \tag{5} \]

$t$ is the time in the detector frame and $F_+,\times$ are called the antenna pattern functions \[23\]. $h(t)$ depends on the detector position and on the signal parameters, which are the sky location of the source of the signal, the signal’s frequency defined at the solar system barycenter at some fiducial time, its first time derivative and four further parameters related to the amplitude and polarization: the intrinsic strain $h_0\,$, the initial phase constant $\phi_0\,$, the inclination angle $\iota$ of the spin axis of the star to the line of sight and the polarization angle $\Psi\,$. These last four parameters are analytically maximized over, leaving only four parameters for which to explicitly search: the right ascension, declination, frequency and spindown.

Since the search covers only a single sky position, the right ascension and the declination are fixed to the coordinates given in Eq. (4). The search templates are arranged in a rectangular grid in frequency and spindown. The result of the matched filter stage is a $2\mathcal{F}$ value for each segment and each template. The incoherent combination of the segments consists of summing a $2\mathcal{F}$ value from each segment and then dividing by the number of segments to obtain the average. By appropriately choosing which values to sum, the incoherent combination performs a refinement in spindown by a factor of $O(1000)$ with respect to the coherent spindown grid. The result is a value of $(2\mathcal{F})$ for each point in this refined parameter space. The search technique does not require refinement in frequency.

The search is performed on the ATLAS cluster at the Max Planck Institute for Gravitational Physics in Hanover, Germany. The parameter space contains a total of $N = 4.4 \times 10^{12}$ templates and is divided among 10,678 jobs, each covering a different frequency band and a range in spindown values from $-f_{\text{max}}/200$ yr $\leq f' \leq 0$ Hz/s, where $f_{\text{max}}$ is the upper frequency of the band for each job. The frequency bands become smaller and smaller as the frequency increases in such a way that the computation time is about constant and equal to about $\sim$5 hours on an Intel® Xeon® CPU X3220@2.40 GHz. Each job returns the values of the detection statistic at the most significant 100,000 points in parameter space.

D. Postprocessing

The search returns results from 1,067,800,000 points in parameter space. With the postprocessing we subject these candidates to a set of vetoes aimed at removing the ones stemming from disturbances, reduce the multiplicity by clustering the ones that are not independent from one another, and zoom in on the most significant subset of these.

The first step is the removal of all candidates that have frequencies within bands that are known to be contaminated by spectral artifacts. Various disturbances affect the data, like mechanical resonances and electrical components of the detectors, and may result in enhanced $(2\mathcal{F})$ values. Many of these spectral disturbances are well known
(see Tables VI and VII of [14]), and we discard candidates that stem from the analysis of potentially contaminated data, which leaves us 889,650,421 candidates (~83.3%).

Because of the low mismatch of the search grids, a detectable signal would produce significant values of the detection statistic in parameter space cells neighboring the actual signal location. In the second postprocessing step, we cluster candidates that could be ascribed to the same signal and associate with the cluster the value of its most significant candidate. Based on results of Monte Carlo studies, we pick a fixed rectangular cluster of \(2 \times 25\) frequency \(\times\) spindown bins, which is large enough to enclose parameter space cells with detection statistic values down to half of the maximum of the detection statistic of a real GW candidate. After the application of this clustering procedure, we are left with 296,815,037 candidates (~33.3% from previous stage).

To confirm that a high \(\langle 2F \rangle\) value is the result of a GW signal, the signal must show consistent properties in the data from both detectors. A very simple but efficient veto used in previous searches [14] compares the outcome of single and multidetector \(\langle 2F \rangle\) values and identifies candidates stemming from local disturbances at one of the detector sites. In a false dismissal study, 500 simulated signals all passed. This veto removes ~11.8% of the candidates surviving from the previous stage.

The next signal consistency check is computationally time consuming, and hence we do not apply it to the whole set of 261,655,549 candidates that survive up to this stage. Rather, we apply it only to the subset of candidates that could potentially show up as statistically significant in a follow-up search. This allows us to keep candidates whose \(\langle 2F \rangle\) value is significantly below what we expect for the loudest from the entire parameter space search on Gaussian noise.\(^2\)

The probability density \(p^\text{loudest}(\langle 2F \rangle|N)\) for the largest summed \(2F\) value over \(N\) independent trials, \(2F^*\), is [4]

\[
p^\text{loudest}(\langle 2F \rangle|N) = Np(\chi^2_{4 \times 630}; 2F*) \times \left[ \int_0^{2F*} p(\chi^2_{4 \times 630}; 2F) d(2F) \right]^{(N-1)},
\]

where \(\chi^2_{4 \times 630}\) denotes a \(\chi^2\) statistic with \(4 \times 630\) degrees of freedom. The expected value of the largest detection statistic value over \(N = 4.4 \times 10^{12}\) independent trials simply is

\[
E[2F^*] = \int_0^{\infty} 2F^* p^\text{loudest}(2F^*|4.4 \times 10^{12}) d(2F^*),
\]

which yields a value of 4.88 with a standard deviation of less than 0.03. The \(N\) templates are not independent, and Eq. (7) slightly overestimates the actual expected value. A fit of the actual distribution suggests that the number of effective independent templates is \(N_{\text{eff}} \sim \frac{N}{2}\). This moves the actual distribution of \(p(\langle 2F \rangle)\) towards lower values of \(\langle 2F \rangle\), increasing the actual significance of candidates. We set the threshold to \(\langle 2F \rangle_{\text{thr}} = 4.77\), which reduces the number of candidates to 27,607. The 4.77 threshold corresponds to more than 3.5 standard deviations below the expectations for the loudest over the entire search in Gaussian noise for \(N_{\text{eff}}\) as low as \(\frac{N}{4}\) and to 4 standard deviations below the expectations for \(N_{\text{eff}}\) templates.

The next veto is based on the idea that for a real signal the signal-to-noise ratio would accumulate steadily over the 630 segments, rather than be due to the high contribution of a few single segments. In contrast, noise artifacts are often limited to shorter durations in time, and hence influence the \(\langle 2F \rangle\) values only within a limited number of segments. To detect candidates with such a behavior, the average \(\langle 2F \rangle\) value is recomputed omitting the contribution from the highest \(2F\) over the 630 segments. A candidate is rejected if its recalculated \(\langle 2F \rangle\) is lower than \(\langle 2F \rangle_{\text{thr}}\). This veto has a false dismissal rate of 0.8% over 500 trials. There are 1138 candidates that survive this veto. Of this set, about 90% can be ascribed to the hardware-injected pulsar 3 (see Appendix A), leaving 59 candidates, of which 20 are several standard deviations above what is expected for the loudest. Only a more sensitive follow-up search could shed light on the nature of these.

We follow up the surviving 59 candidates with a coherent search spanning \(T_{\text{coh}} = 90\) days of data from the H1 and L1 detectors between February 1, 2007, 15:02:57 GMT and May 2, 2007, 15:02:57 GMT. The data set was again chosen based on the sensitivity to a CGW from the GC. It contains a total of 6522 half-hour baseline SFTs (3489 from H1 and 3033 from L1), which is an average of 67.9 days from each detector. The resolution in frequency and spindown is derived from the time spanned,

\[
df_{\text{coh}} = (2T_{\text{seg,coh}})^{-1}, \quad df_{\text{coh}} = (2T_{\text{seg,coh}}^2)^{-1}.
\]

The resolution in spindown turns out to be comparable to the fine grid resolution of the initial search. The frequency resolution is much finer. The covered frequency and spindown ranges are

\[
\Delta f = 5 df = 5T_{\text{seg}}^{-1}, \quad \Delta \dot{f} = 11 df_{\text{fine}} = 11T_{\text{seg}}^{-2}.
\]

Centered around the frequency and spindown of the candidate to follow up. These ranges are chosen because the parameters of the highest recovered \(\langle 2F \rangle\) are always within a distance of two frequency bins and five spindown
IV. RESULTS

We place 90% confidence frequentist upper limits (ULs) on the maximum intrinsic GW strain, $h_0^{90\%}$, from a population of signals with parameters within the search space, based on the loudest candidate from the search that could not be discarded as clearly not being of astrophysical origin. In particular, the upper limits refer to 3000 portions of the frequency-spindown parameter space with equal number of templates of about $1.5 \times 10^5$. They refer to sky positions within $\sim 3$ pc distance of Sgr A*, and to uniformly distributed nuisance parameters $\cos \iota$, $\phi_0$ and $\Psi$. $h_0^{90\%}$ is the CGW amplitude such that 90% of a population of signals would have yielded a more significant value of the detection statistic than the most significant measured by our search in that portion of parameter space. The 90% confidence includes the effect of different realizations of the noise in the band and of different signal shapes (different combinations of $\cos \iota$, $\phi_0$, $\Psi$, $f$, $f$, $\alpha$, $\delta$) over the sub-band parameter space. This is a standard upper limit statement used in many previous searches, from [35] to [14]. We exclude from the upper limit statements frequency bands where more than 13% of the parameter space was not considered due to postprocessing vetoes (this reduces the UL bands to 2549 bands). The choice of 13% was empirically determined as a good compromise between not wanting to include in the UL statements frequency bands where the searched parameter space had been significantly mutilated and wishing to keep as many valid results as possible. Ten further frequency bands were excluded from the upper limit statements.

These bands are at neighboring frequencies to strong disturbances and are themselves so disturbed that our upper limit procedure could not be applied to these frequency bands. Figure 1 shows the upper limit values. The tightest upper limit is $-3.35 \times 10^{-25}$ at $\sim 150$ Hz. The large value upper limit values close to 350 Hz are due to the residual spectral of the detectors’ violin modes.

Assuming a nominal value for the moment of inertia, the upper limits on $h_0$ can be recast as upper limits on the pulsar ellipticity, $e^{90\%}$. Figure 2 shows these upper limits for values of the moment of inertia between 1 and 3 times the fiducial value $I_{\text{fid}} = 10^{38}$ kg m$^2$. The upper limits range from $6.2 \times 10^{-3}$ at 78 Hz to $2.7 \times 10^{-3}$ at 496 Hz for $I_{\text{fid}}$. The most constraining value is $8.7 \times 10^{-6}$ at 496 Hz for $3 \times I_{\text{fid}}$.

Following [36], the upper limits can also be translated into upper limits on the amplitude of r-mode oscillations, $\alpha^{90\%}$, as shown in Fig. 3. The upper limits range from 2.35 at 78 Hz to 0.0016 at 496 Hz.

FIG. 1. This plot shows the 90% confidence upper limits on the intrinsic GW strain $h_0$ from a population of signals with parameters within the search space. The tightest upper limit is $-3.35 \times 10^{-25}$ at $\sim 150$ Hz. The large value upper limit values close to 350 Hz are due to the residual spectral of the detectors’ violin modes.

FIG. 2. This plot shows the 90% confidence upper limits on the ellipticity $e$ for our target population of sources, at a distance $r = 8.3$ kpc and for three different values for the moment of inertia.
FIG. 3. This plot shows the 90% confidence upper limits on the amplitude $a$ of $r$-mode oscillations.

V. CONCLUSION

Although this is the most sensitive directed search to date for CGWs from unknown neutron stars, no evidence for a GW signal within 3 pc of Sgr A* was found in the searched data. The first upper limits on gravitational waves from the GC were set by [37], a search analyzing the data of the resonant bar detector EXPLORER in the frequency range 921.32–921.38 Hz. The sensitivity that was reached with that search was $2.9 \times 10^{-24}$. More recent upper limits on permanent signals from the GC in a wide frequency band (up to 1800 Hz) were reported by [38]. A comparison between the results of [38] and the upper limits presented here is not trivial, because the upper limits set in [38] refer only to circular polarized waves, while our results refer to an average over different polarizations. Also, the effect of frequency mismatch between the signal parameter and the search bins is not folded in the results of [38], whereas it is for this search. A further difference is that the upper limits of [38] are Bayesian, while the results presented here are given in the frequentist framework. Taking these differences into account, we estimate that within a 10% uncertainty our results tighten the constraint of [38] by a factor of 3.2 in $h_0$. The tightest all-sky $h_0$ upper limit in the frequency range 152.5–153.0 Hz from [14] is $7.6 \times 10^{-25}$. The results presented here tighten the [14] constraint by about a factor of two. This improvement was possible because of the longer data set used, the higher detection efficiency of this search that targets only one point in the sky, and the comparatively low number of templates. For comparison, the targeted search for a CGW signal from Cas A, which used 12 days of the same data as this search and analyzed them with a fully coherent method, resulted in a 95% confidence at $\sim 150$ Hz of $7 \times 10^{-25}$ [4]. The improvement in sensitivity compared to the search of [4] is gained by having used much more data and low-threshold postprocessing.

Following [14,39] we express the GW amplitude upper limits as $h_0^\text{90\%} = H \sqrt{S_h}/T_{\text{data}}$, where $S_h$ is the detector noise and $T_{\text{data}} = N_{\text{seg}} T_{\text{seg}}$. The factor $H$ can be used for a direct comparison of different searches, with low values of $H$ implying, at fixed $\sqrt{S_h}/T_{\text{data}}$, a more effective search [40]. This search has a value of $H \sim 77$, which is an improvement of a factor 2 compared to [14], where $H$ varies within $\sim 141$ and $\sim 150$ with about half of the data. This confirms that the improvement in sensitivity for this search with respect to [14] can be ascribed to an overall intrinsically more sensitive technique being employed, for the reasons explained above.

This search did not include nonzero second-order spindown. This is reasonable within each coherent search segment: the largest second-order spindown that over a time $T_{\text{seg}}$ produces a frequency shift, $\dot{f} T_{\text{seg}}^2$, that is less than one half of a frequency bin is

$$\dot{f} T_{\text{seg}}^2 \leq \frac{1}{2T_{\text{seg}}}. \quad (10)$$

Inserting $T_{\text{seg}} = 11.5$ h, the maximum-second-order spindown that satisfies Eq. (10) is $\dot{f} \sim 7 \times 10^{-15}$ Hz/s$^2$. Using the standard expression for the second-order spindown,

$$\dot{f} = n \dot{f}_. \quad (11)$$

and substituting $|\dot{f}/f| = 1/200$ yr, a braking index $n = 5$, and $\dot{f}_. = -7.86 \times 10^{-8}$ Hz/s (the largest spindown covered by the search) implies that the highest $\dot{f}$ that should have been considered is $\dot{f} \sim 6 \times 10^{-17}$ Hz/s$^2$. We conclude that for the coherent searches over 11.5 hours, not including the second-order spindown does not preclude the detection of systems in the covered search space with second-order spindown values less than $\sim 6 \times 10^{-17}$ Hz/s$^2$. Due to the long observation time (almost two years), the second-order spindown should, however, not be neglected in the incoherent combination. The minimum second-order spindown signal that is necessary to move the signal by a frequency bin $\delta f$ within the observation time is

$$\dot{f}_\text{min} = \frac{\delta f}{T_{\text{obs}}} \sim 6 \times 10^{-21} \text{ Hz/s}^2. \quad (12)$$

This means the presented results are surely valid for all signals with second-order spindown values smaller than $6 \times 10^{-21}$ Hz/s$^2$. Computing the confidence at a fixed $h_0^\text{90\%}$ value for populations of signals with a second-order spindown shows that signals with $\dot{f} \leq 5 \times 10^{-20}$ Hz/s$^2$ do not impact the results presented in this work. This value is larger than all reliably measured values of known neutron stars as of today, where the maximum value measured is $\dot{f} \approx 1.2 \times 10^{-20}$ Hz/s$^2$ [17].

However, the standard class of signals with large spindown values is expected to also have high values of the second order spindown [Eq. (11)]. Not having included a
second-order spindown parameter in the search means that not a standard class of objects but rather a population with apparently very low braking indices is targeted. Such braking indices are anomalous, i.e., it would be surprising to find such objects; however, they are not fundamentally impossible and could appear, for example, for stars with either a growing magnetic surface field or a growing moment of inertia [41]. Under these circumstances the relationship between observed spindown and ellipticity may break down. The ellipticity of the star might be large enough that gravitational waves, even at a distance as far as the GC, can be measured at a spindown value that would not imply such strong gravitational waves in the standard picture. This is an important fact to keep in mind when interpreting or comparing these results.

For standard neutron stars, the maximum predicted ellipticity is a few times $10^{-3}$ [42]. The upper limits on $\epsilon$ presented here are a factor of a few higher than this over most of the searched frequency band and for $I_{\text{fid}}$. Exotic star models do not exclude hybrid or solid stars, which could sustain ellipticities up to a few $10^{-4}$ or even higher [43–45], well within the range to which our search is sensitive. However, since the predictions refer to the maximum values that model could sustain, they don’t necessarily predict those values, and hence our nondetections do not constrain the composition of neutron stars or any fundamental property of quark matter. We have considered a range of variability for the moment of inertia of the star between 1–3 $I_{\text{fid}}$. Reference [46] predicts moments of inertia larger than $I_{\text{fid}}$ for stars with masses $\gtrsim 1 M_\odot$, which means for all neutron stars for which the masses could be measured. Reference [47] has estimated the moment of inertia for various equations of state (EOS) and predicts a maximum of $I = 2.3 \times I_{\text{fid}}$. Reference [48] found the highest moment of inertia to be $I = 3.3 \times I_{\text{fid}}$ for EOS G4 in [49].

For frequencies in the range 50–500 Hz, the lower limits on the distance derived in [14] at the spindown limit range between 0.5 and 3.9 kpc, but because of the smaller spindown range the corresponding spindown ellipticities are lower, down to $7 \times 10^{-6}$ at 500 Hz, with respect to the ellipticity upper limit values that result from this search. This reflects a different target population: closer by, and with lower ellipticities in [14], farther away, at the GC, and targeting younger stars in this analysis. We note that the $h_0^{90\%}$ upper limits presented here could also be reinterpreted as limits on different ellipticity-distance values (as done in Fig. 13 of [13]) for sources lying along the direction to the GC.

At the highest frequencies considered in this search, $\alpha^{90\%}$ reaches values that are only slightly higher than the largest ones predicted by [50]. We stress that the uncertainties associated with these predictions are large enough to encompass our results.

The main uncertainty affecting the prospect for detection of CGWs as the ones targeted by this search is the ellipticity of the source, whose possible values span many orders of magnitude, from $10^{-3}$ to $10^{-17}$ and lower. Because of this, no detection is guaranteed, not with the tenfold sensitivity improvement of the second generation of GW detectors (Advanced LIGO [51], Advanced Virgo [52,53], KAGRA [54]) and not even with the third-generation detectors (e.g., Einstein telescope [55]). However, since there is no fundamental constraint for the maximum ellipticity to be lower than $10^{-5}$, it is plausible to assume that objects do exist with ellipticities in the range $10^{-6}$–$10^{-5}$. This is a range that will be accessible, and partly already is, to gravitational wave detectors for objects at the GC, which clearly is a promising region to search because of its richness of neutron stars.

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**APPENDIX: HARDWARE INJECTIONS**

Over the course of the S5 run, ten simulated pulsar signals were injected into the data stream by physically
exciting the detectors’ mirrors. Most of these fake pulsars have sky locations far away from the GC, but one of them is close enough that it contributes to the \(\langle 2\mathcal{F} \rangle\) values of the templates in our search that are close to the injection parameters. The parameters of this hardware-injected signal are shown in Table I. The distance between that hardware injection and the GC position is \(\sim 1.537\) rad in right ascension and \(\sim 0.077\) rad in declination. This is not within the covered parameter space. Nevertheless, the injected signal is so strong—the plus- and cross-polarization translate into an implied \(h_0 \sim 1.63 \times 10^{-23}\) which is a factor of \(\sim 40\) louder than our \(h_{10}\) at 108 Hz—that even a relatively marginal overlap with a template produced a significant \(\langle 2\mathcal{F} \rangle\) value. This pulsar is detected with this search, even though it lies outside the defined parameter space.

### Table I. The parameters of the hardware injection that was detected with this search.

| Value | Property |
|-------|----------|
| 751680013 | Pulsar \(t_{\text{ref}}\) in SSB frame [GPS sec] |
| \(3.2766 \times 10^{-20}\) | Plus-polarization signal amplitude |
| \(-5.2520 \times 10^{-21}\) | Cross-polarization signal amplitude |
| 0.444280306 | Polarization angle |
| 5.53 | Phase at \(t_{\text{ref}}\) |
| 10.8571594 | GW frequency at \(t_{\text{ref}}\) [Hz] |
| \(-0.583578803\) | Declination [rad] |
| 3.113188712 | Right ascension [rad] |
| \(-1.46 \times 10^{-17}\) | First spindown parameter \([df_0/dt]\) |
| 0.0 | Second spindown parameter \([df_0/dt^2]\) |
| 0.0 | Third spindown parameter \([df_0/dt^3]\) |

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