Comparison of lithium niobate and silicon substrate on phase shift and efficiency performance for mach-zehnder interferometer modulator

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ABSTRACT
In this study, the low-group velocity slow-light mach-zehnder interferometer (MZI) modulator, low loss and high efficiency for two modulator substrate lithium niobate (LN) and silicon were presented and optimized at 1.55µm operating wavelength. The high power consumption of conventional modulator was the major drawback in the operation of modulators. Therefore, it was a good time for low-power modulator design and development and to compare the LN and Silicon modulator on the phase shift using the slow-light technique by designing the full MZI modulator consisting of splitter and combiner on both substrates. The phase shift of LN is 2% compared with the silicon 0.09% and higher phase shift give better performance with low power consumption due to the change of modulating voltage of the MZI modulator for LN while the silicon depends on modulating voltage manipulating concentration of charge carrier in doped silicon.

Keywords: Group velocity, Lithium niobate, Mach-zehnder interferometer, Optical modulator, Slow-light

1. INTRODUCTION
Nowadays, there has been rapid and fast enhancement of the computer chip performance and a reduction in individual components size. However, most electrical interconnects, which carry data inside the microprocessors and between the processor and memory have drawbacks of high loss, low efficiency and high power consumption [1, 2]. Traditional optical interconnect systems consist of optical waveguide and optic-electric/electro-optic (OE/EO) conversion devices, in order to achieve the multi-level modulation formats which are commonly used for high-speed transmission systems. Thus, accuracy of OE conversion is very important as well as the efficiency of conversion and response time of such device [3-5]. However, optical interconnects still remains difficult to be optimized, due to the lack of suitable material and modulation mechanisms [6]. Therefore, in this paper we discuss the design of the photonic crystal waveguide with different substrate of lithium niobate (LN) and silicon materials.

The LN electro-optic modulators have been the optoelectronic industry’s workhorse for the decades [7-9], however, it is difficult to be integrated on-chip due to difficulties and complications in the fabrication process. Currently, disadvantages of LN modulators are bulky, costly, restricted bandwidth, high drive voltages and also unable to achieve the full potential of materials [10-12]. Future of the photonic systems
requires modulators with a CMOS-compliant drive voltage, large bandwidth, low insertion loss, excellent signal quality and compatibility with large-scale manufacturing. Although the material of LN is difficult to incorporate there are other photonic material that are compatible with the fabrication process such as silicon, which have good potential for integration with CMOS electronics [13-15], for example low drive voltages and high bandwidth polymers [16, 17]. A main material for high-speed EO conversion in modulator is silicon mach-zehnder optical modulators [18, 19].

Nowadays, the system operates at bit rates that surpass bit rates of 100Gb/s. The optical signal is demanded to have high speed and bandwidth for future and potential networks [20, 21]. Some developments of optical networks with the use of the mach-zehnder interferometer (MZI) modulator were presented [22]. MZI is the device that used to calculate the relative phase shift between two beams of light source either by changing the length of one arm or by putting a sample in one the arm by biasing due to high power consumption that needs to be removed. The effects of the high power in the MZI modulator can lead to high group velocity and losses. One at the input acts as a splitter and at the output acts as a combiner. At the output, the light is split into two and merges. The optical path length of two arms allows the phase shift according to delay to into the wavelength of the input signal. This property is used to design the number of optical devices used in the all-optical domain for signal processing [23]. In previous research the Y-structure show the phase shift of 2.08 rad [24]. Higher phase shift gives a better performance of the device. This research shows higher phase shift by numerically analyze the the phase shift of the device, and the transmission efficiency of the combiner is above 70% with the step taper [25]. The coupling efficiency was enhanced and the transmission of the modulator was improved.

In this article, there was a theoretical study of two types of material of the MZI modulator and photonic crystal waveguide (PCW) that are LN and silicon. Both modulators worked at 1.55µm of communication wavelength. For these designs we were able to examine the slow light and the group velocity in both PCW of different materials and the phase shift of one arm of MZI by the variation of the refractive index, RI. In addition, the simulation results showed that the enhancement and improvement for both of MZI modulators with different types of material and the phase shifted has been improved to achieve better performance of the device. The MZI modulator can be commonly used in on-chip for the optical interconnect applications and as well as for the embedded devices for example in photonic crystal cavities.

2. **RESEARCH METHOD**

Figure 1(a) shows the full schematic and Figure 1(b) schematic design of the MZI modulator of LN photonic crystal cavities consisting of three parts which are splitter, PCW and combiner. By etching the air holes, the photonic crystal waveguide is structured. L represents the length of the modulator and the total length of the modulator is L1+2L2. The length of the splitter and combiner are the same length. Both the Y shape and the waveguide bend are built for the splitter and combiner parts. The slow light method is applied by both arms of the MZI modulator via the L1 length of the slow light waveguides. All the three electrodes are located in the waveguide line of slow light, these electrodes are similar to the waveguides of slow light, and there is an EO response effect on LN. The voltage, U is applied to the center electrode that can produce a voltage wave. Both external electrodes are to the ground. The incident light is polarized transverse electric (TE). The waveguide is designed to eliminate one row of the air holes in the perfect PCW for both of the materials that are LN and silicon as in Figure 2. The photonic crystal waveguide holes radius R=0.32a the thickness of the slab, h=362nm and lattice constant, a=0.654. The optimization of the MZI modulator can be seen in the following parts for both materials.

![Figure 1. (a) The full schematic design of the LiNbO3 photonic crystal cavity-based MZI modulator, (b) The schematic design of the PCW slow-light implementation for both LiNbO3 and silicon materials](image-url)
For both PCW models with the various materials, we introduce slow light techniques in the photonic crystal waveguide. According to the optical theory the group index \( n_g \) of slow light, showing the slowdown factor compared to the speed of light in vacuum \( c \), is given by \( n_g = \frac{c}{V_g} = \frac{d k}{d \omega} \) where \( k \) and \( \omega \) are the wave number and angular frequency respectively [26, 27]. This means that the slow light is due to the large first-order dispersion \( \frac{d k}{d \omega} \). Furthermore, the slow light is limited by the delay-bandwidth product written as \( n_g(\Delta \omega/\omega) = n_g(\Delta \lambda/\lambda) = \Delta n \), where \( \Delta \omega \) and \( \Delta \lambda \) are the frequency and wavelength bandwidth of slow light, respectively and \( \Delta n \) is the effective refractive index change in material or structure within the bandwidth [28, 29]. This relationship implies that, one cannot expect a large \( n_g \) independently of the bandwidth. If one is considering any application of slow light, the bandwidth needed for the target application should first be calculated and the maximum \( n_g \) from the above equation estimated.

3. RESULTS AND DISCUSSION

The complete of TE propagation information of the perfect photonic crystal for LN is shown in Figure 2(a). It shows the existing band gap between 0.39 and 0.46 below the light line and is determined to solve the Maxwell equations using the plane wave expansion (PWE) technique. Figure 2(b) is the measured band gap for silicon which is in between 0.25 and 0.38. The photonic band gap of the main propagation mode is shown in Figure 2(c) by the (blue line) of the signal line defect PCW, which supports the lossless even mode. The slow light of PCW support a low group velocity, \( V_g \) where a flat group velocity dispersion region. However, left out the dispersion of slow light in LN can cause the signal waveform to be influenced by excessive group velocity dispersion and signal distortion. It can also affect the performance for both PCW materials in optical interconnect applications. The implication changes the radius of the holes of PCW to the amount of the flat signal of low group velocity dispersion region. The band diagram and the gap between 0.36 and 0.46 when \( r = 0.32a \) and \( a = 0.6 \) is shown as in Figure 2(c).

\[
\Delta n = \frac{n^3 L N \gamma_{33} U}{2d}
\]  

(1)

Where \( n_{LN} \) the extraordinary refractive index, RI which represents the nonlinear EO coefficient, \( U \) is the applied voltage, and \( d \) is for the gap between the electrodes. To measure the phase shift this depends on the applied voltage;

\[
\Delta \phi = \frac{2\pi}{\lambda} \Delta n \cdot L
\]  

(2)

Where \( \lambda \) is the wavelength, \( \Delta n \) represents the index change, and \( L \) refers to the length of the region with which the electrical field is applied. When the applied voltage is applies differently so that the index changes also change, such that the calculated refractive index changes also change. If the refractive index changes the simulation results show that even with a small change, the group velocity and loss change. The group velocity modifies the slow light technique occur and give the phase shifted. The MZI modulator has
two arms, in order to determine the refractive index both arm using the formula where for the upper arm $n_{LN} - |\Delta n|$ and the lower arm $n_{LN} + |\Delta n|$, when $|\Delta n|$ is 0.00331 for 0.66 V and $|\Delta n|$ is 0.00662 is for 1.32V, the simulation results as shown Figure 2. The phase shift for 0.66 V is 1.22892 rad while for the applied voltage of 1.32 V is 2.45784rad. Other properties of the mode, such as group velocity and loss, can also be determined in addition to calculating the band structure. As the group velocity reduces, the loss increases. $R=0.32$ $a=0.192$, and $a=0.6$. The refractive index for the applied voltage of 0.06V is $n=2.13969$ and the refractive index of 1.32 V is $n=2.13638$, both of which are determined using the formula in Figure 3.

![Band structure](a)

![Band structure](b)

![Group velocity vs kx](c)

![Group velocity vs kx](d)

![Loss vs kx](e)

![Loss vs kx](f)

Figure 3. The measured effects of the LN simulation with various voltages. (a), (c), (e) with respect to 0.06V and (b), (d), (f) with respect to 1.32V

The modulation principle for the silicon material as shown in Figure 4 is based on the free carrier dispersion effect and the relationship between the index perturbation and carrier concentration perturbation by the following function when the wavelength of incident light $\lambda=1.55\mu m$.

$$\Delta n = \Delta n_e + \Delta n_h = -[8.8x10^{-22}(\Delta Ne)+8.5x10^{-18}(\Delta Nh)0.5]$$

(3)

$\Delta n_e$ and $\Delta n_h$ are the refractive index changes caused by the changes of the electrons and holes concentrations respectively. $\Delta n_e$ and $\Delta n_h$ are the changes of electron and hole concentrations respectively. The change of the refractive index will measure the refractive index for both arm of the MZI modulator where for the upper arm $n_{si} - |\Delta n|$ and for the lower arm $n_{si} + |\Delta n|$ where $n_{si}$ is the refractive index of silicon. Then we try the different of carrier concentrations for holes and electrons $(\Delta Ne)e =1x10^{15}cm^2$ and
(ΔNh)c = 4x10^{15} \text{ cm}^{-2} \text{ and for the second carrier concentration is } (ΔNe)c = (ΔNh)c = 3x10^{17} \text{ cm}^{-3} \text{ From the change of the refractive index we can calculate the phase shifted by this formula, } Δ∅ = \frac{2π}{λ} Δn L. \text{ The phase different for the first concentration after the measurement } Δ∅ \text{ is 0.00989 and the second is 0.09802. The first phase different is smaller than the second phase different. This is because the phase different depends on the carrier concentrations.}

Figure 4. The results show the different of the carrier concentration for the silicon. (a), (c), (e) for (ΔNe)c = 1x10^{15} \text{ cm}^{-2} \text{ and (ΔNh)c = 4x10^{15} \text{ cm}^{-2} } \text{ and (b), (d), (f) for (ΔNe)c = (ΔNh)c = 3x10^{17} \text{ cm}^{-3} } \text{Figure 5 the optimized schematic of photonic crystal splitter-combiner with the designated holes determines the holes where the radius or position changes. The lattice constant of LN a=0.6 and r = 0.192 while for silicon a=0.5 and r = 0.2. In order to obtain the good and better efficiency, the radius and position of holes are selected. Figure 6 shows the steady state electric field figure for TE-polarized wave propagation through an optimized splitter configuration at 1.55\text{µm} \text{ wavelength where the wavelength range is between 1.43-1.67µm and the band gap for the combiner of the MZI modulator with the same of lattice constant and radius of the cavities for LN. The steady state electric field figure for the TE-polarized wave propagation for silicon through an optimized splitter configuration at 1.55µm wavelength where the wavelength range is between 1.3-1.98µm and the band gap for the combiner of the MZI modulator with the same of lattice constant and radius of the cavities.
Figure 7 shows the result of the untapered of PCW with all same radius of the holes where $R=0.192$ for LN and $R=0.2$ for the silicon in the wavelength range (1.53$\mu$m-1.57$\mu$m). The optimization applied the gaussian modulated continuous wave of the input field transverse. The total efficiency of the output splitter and combiner for the LN material are 65% and 18% and the total efficiency of the output for the splitter and combiner for the silicon material are 40% and 4% at 1.55$\mu$m operating wavelength. This means that the output efficiency on the combiner for the silicon is higher compared to LN due to the loss of the wave propagation through the MZI modulator waveguide. The radius of all holes for both LN and silicon materials are fixed as mentioned in Figure 6.

Figure 5. The optimized schematic design of the PCW splitter-combiner MZI modulator

Figure 6. The band diagram and transmission for the (a) LN and (b) for the silicon materials

Figure 7. The transmission efficiency performance for the splitter of LN and silicon (a) and (b). The transmission efficiency performance for the combiner of LN and silicon (c) and (d)
Figure 8 shows the results of tapered PCW transmission for the optimized splitter and combiner in the wavelength range (1.53µm-1.57µm). The total efficiency of the output splitter and combiner for the LN material are 50% and 89% and the total transmission of the output splitter and combiner compared to the previous research are 40% and 70% and for the silicon material are achieved 55% and 18% at 1.55µm operating wavelength. This means that the output transmission at the combiner for the LN is higher compared to the silicon due to the loss of the wave propagation through the mzi modulator waveguide when the parameters of the designated cavities are defined r1= 0.763a, r5= 0.436a, r2= 0.218a, dy1= 0.109a, and dy2= 0.218a. Then the parameters numbered holes for silicon are r1= 0.6a, r5= 0.36a, r2= 0.2616a, dy1= 0.1308a, and dy2= 0.2616a. Then Table 1 shows the comparison of LN and silicon MZI modulator.

![Figure 8. The calculated transmission efficiency performance for the splitter of LN and silicon (a) and (b). The transmission efficiency performance for the combiner of LN and silicon (c) and (d)'][2]

Table 1. The comparison of Lithium Niobate and Silicon MZI modulator

| Materials       | Group velocity (Vg)                     | Calculation            | Efficiency (%) |
|-----------------|----------------------------------------|------------------------|----------------|
| Lithium Niobate | depends on the change of the refractive index where (Refractive index, RI vs. Voltage) | \( \Delta n = - \frac{n^3 \Delta n U}{2d} \) | The percentage of the output splitter and combiner for the LN is 65% and 18% of untapered PCW. Then the percentage of the output splitter and combiner for the LN is 50% and 89% of tapered PCW. |
| Silicone        | depends on the carrier concentration of holes and electrons | \( \Delta n = \Delta n e + \Delta n h \approx \frac{8.8\times10^{-16}(\Delta n e)+8.5\times10^{-16}(\Delta n h)0.5}{5} \) | The percentage of the output splitter and combiner for the silicon is 40% and 4% of untapered PCW. Then the percentage of the output splitter and combiner for the silicon is 55% and 18% of tapered PCW. |

4. CONCLUSION

The study is related to the comparison of the performances on different materials MZI modulator which are LN and silicon material. Modulator performance is studied on a photonic crystal waveguide based on optimization using the OptiWave software. The MZI modulator of LN gives the highest phase shift which is 2.45784 rad and it gives the better performance and the attain the set of slow light waveguides that supports a low group velocity over a flat signal group velocity region. The percentage of the splitter is 50% and combiner is 89% optimized MZI modulator design LN material used. With tapered techniques or methods, the transmission is greatly improved about 70% for the LN MZI modulator compared to the previous research for the photonic device application based on the photonic crystal properties and design.

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