Abstract

We present Fabry-Pérot interferometric observations of the narrow Hα component in the shock front of the historical supernova remnant Tycho (SN 1572). Using GHαFaS (Galaxy Hα Fabry-Pérot Spectrometer) on the William Herschel Telescope, we observed a great portion of the shock front in the northeastern (NE) region of the remnant. The angular resolution of ~1″ and spectral resolving power of R~21,000 together with the large field-of-view (3.4′×3.4′) of the instrument allow us to measure the narrow Hα-line width in 73 bins across individual parts of the shock simultaneously and thereby study the indicators of several shock precursors in a large variety of shock front conditions. Compared to previous studies, the detailed spatial resolution of the filament also allows us to mitigate possible artificial broadening of the line from unresolved differential motion and projection. Covering one quarter of the remnant’s shell, we confirm the broadening of the narrow Hα line beyond its intrinsic width of ~20 km s^{-1} and report it to extend over most of the filament, not only the previously investigated dense 'knot g'. Similarly, we confirm and find additional strong evidence for wide-spread intermediate-line (~150 km s^{-1}) emission. Our Bayesian analysis approach allows us to quantify the evidence for this intermediate component as well as a possible split in the narrow line. Suprathermal narrow line widths point toward an additional heating mechanism in the form of a cosmic-ray precursor, while the intermediate component, previously only qualitatively reported as a small non-Gaussian contribution to the narrow component, reveals a broad-neutral precursor.

1 Introduction

The main spectral characteristic of Balmer-dominated shocks (BDSs) is a two-component Hα line. Components are produced in radiative decays of excited atoms (Chevalier et al., 1980), whereas cold hydrogen atoms (the ones overrun by the shock) produce a narrow component (~10 km s^{-1}) and broad-neutrals generate a broad component (~1000 km s^{-1}). Broad-neutrals are formed in a charge exchange (CE) process between a cold atom and a hot proton downstream of the shock. BDSs are an important diagnostic tool for shock parameters (Heng, 2010): narrow (broad) component width indicates the pre (post)-shock temperature;
the shock velocity can be estimated from the broad line width and in combination with proper motions of optical filaments provides distance estimates; the electron-to-proton temperature ratio can be constrained from the components’ widths and their intensity ratios. The Hα-line profile is also influenced by possible shock precursors (emissions from the shock interacting with the pre-shock medium), for example cosmic-rays (CRs) and broad-neutral precursors. Heating in the CR precursor results in a narrow Hα component broadened beyond the normal $10–20 \text{km s}^{-1}$ gas dispersion (Morlino et al., 2013). Furthermore, CRs transfer also momentum to the pre-shock neutals introducing a Doppler shift between the pre- and post-shock gas (Lee et al., 2007). CE in the broad-neutral precursor introduces an additional component to the Hα profile – intermediate component – with the width of $\sim 150 \text{km s}^{-1}$ (Morlino et al., 2012).

The Hα-line that is broader than the intrinsic $20 \text{km s}^{-1}$ was previously measured in low-spatial resolution data of Tycho (Ghavamian et al., 2000; Lee et al., 2007), and interpreted as a strong indicator of CR production. The same studies reported also on the detection of the intermediate component. However, both analyses focused on the Hα-bright, but very complex ‘knot g’, where multiple or distorted shock fronts can contribute to the measured broadening of the narrow and intermediate Hα line. Just as spatial resolution is crucial to eliminate or reduce the artificial broadening effect of differential projection, extended spatial coverage of the filament can help to ascertain spatially varying shock (and ambient ISM) conditions. For the first time, we provide both of these in our forthcoming analysis. We expand on previous studies also by providing full posterior distributions instead of relying merely on best-fit parameters (line fluxes, centroids and widths), and provide a quantitative assessment of the significance of the intermediate line as well as possible multiple narrow lines (projected shock fronts).

2 Observations and Reduction

The instrument setup of GHoFaS is well suited for our study of spatially and spectrally resolving the narrow Hα line along the Tycho’s NE rim. GHoFaS is very sensitive to gather enough signal-to-noise (S/N) of around 10 within 6.9 h of observations, and its field-of-view (FoV) of $3.4' \times 3.4'$ $(1024^2$ pixels at 0.2″ pixel scale) is large enough to cover roughly one quarter of the whole remnant. The instrument response function is well approximated by a Gaussian with full width at half maximum (FWHM) of $19 \text{km s}^{-1}$ (Blasco-Herrera et al., 2010). The spectral coverage of around $400 \text{km s}^{-1}$ was centered around Hα line and split into 48 channels with a sampling velocity resolution of nearly $8 \text{km s}^{-1}$.

We reduced the data (see Figure [1]) following the standard procedure for GHoFaS data described in (Hernandez et al., 2008). For each exposure we performed a phase- and wavelength-calibration and thereby built a data-subcube (x,y,λ) with 48 calibrated constant-wavelength slices. For each frame (exposure, subcube), we then derived a (relative) astrometric solution, and aligned all frames onto a common coordinate system, before stacking. In order to be able to take the flatfield effect and the effective exposure time into account, and to reconstruct the local background spectrum, we use the series of object-masked frames to build a flatfield- and a background-stack in the same way and in addition to the “raw” data stack (cube). We then use the flatfield (effective exposure time) cube and the background cube to compare the intrinsic emission model with the data cube (see next section).
3 Analysis and Results

Utilizing the large FoV, limiting bin sizes to $>1''$ that corresponds to the seeing conditions, and requiring $S/N \gtrsim 10$ per bin, we were able to extract spectra from 73 spatial Voronoi bins \cite{CappellariCopin2003}. Thus, we are in a position to measure the narrow Hα-line widths across individual parts of the shocks simultaneously, and thereby study the indicators of precursors in a large variety of shock front conditions (see Figure 2). Although we see only $\sim 1\%$ variations between background regions of $25^2$ pixels, for very large bins with their large integrated signal and signal-to-noise, even these small unaccounted-for residuals can become comparable to the noise. Therefore, we exclude bins with an area larger than 400 pixels from the analysis.

We use Bayesian inference to perform parameter estimation – traditionally termed "fitting" – as well as comparison and selection. This choice of method is motivated by our desire to maintain small bins with often low $S/N$, but to simultaneously obtain reliable and complete information about generally significantly non-Gaussian relative probabilities of the parameters ("errors"). This stands in stark contrast to the commonly applied method of deriving some (supposedly) best-fit set of parameters and a rough, generally vastly underestimated, "error bar" via minimizing the chi-square (maximum-likelihood) and calculating its local derivatives. We numerically calculate the posterior parameter probability distributions ("posteriors" for short) via a Markov-Chain Monte-Carlo (MCMC) method, and summarize the posteriors for each bin and model by their global maximum-posterior ("best-fit"), median, and the central 95%-confidence interval limits.

For our purpose, just as important as ascertaining the line parameters is the model comparison (and subsequent selection). We want to determine if, as visual inspection of the spectra and theoretical considerations (precursors, differential shock projection) suggest, a so-called intermediate line (IL) is needed in addition to the narrow line (NL) to properly describe the data, or if the NL is split, i.e. if two centroid-shifted NLs are present. Before comparing any model and its specific parameters with the data, we account for the local flatfield spectrum
Figure 2: Spatial maps of Tycho’s NE filament: contours of 73 Voronoi bins for S/N=10 binning criteria, spatial variation of the intrinsic narrow-line width ($W_{NL}$) in the NL model, IL flux fraction in the NLIL model, and logarithmic evidence ratio of the NLIL relative to the NL model. The white circles are the masked stars.

(effective relative exposure time) and add to it the local background spectrum. Each line (Hα component) is represented by a Gaussian (flux, centroid, width), except for the broad line (BL), which, due to its large width compared to the GHαFaS spectral range, is represented by a constant that also includes the continuum. We consider the following intrinsic models: NL, 2NL, NLNL, NLIL, 2NLIL, NLNLIL, where 2NL and NLNL denote two NLs with common and independent width, respectively.

The prior parameter distributions are flat or nearly so (Beta or Dirichlet distributions with low $\alpha(=\beta) \geq 1$ parameter) – that is, we do not (strongly) prefer any parameter values within the model definition limits. Those limits are [10, 100] km s$^{-1}$ for the NL width (intrinsic FWHM), and for the IL, [100, 350] km s$^{-1}$ as predicted for shock velocities [1500, 3500] km s$^{-1}$ (Morlino et al., 2012, 2013). Figure 3 shows 1D-marginalized posteriors over model NLIL parameters for one of the bins. The vertical red lines show the parameters at the maximum of the posterior (“best-fit” model, the prediction of which is the solid red line in the top-right blue-framed panel). We find the NL width being close to 40 km s$^{-1}$ and IL with the width of $\approx 250$ km s$^{-1}$ comprising 55% of the total flux. Moreover, NL widths in a single-line model (NL model) are larger than 20 km s$^{-1}$ (the second panel in Figure 2), that is they are broadened beyond the expectation when no CR precursor is present. This result is not entirely new (Ghavamian et al., 2000; Lee et al., 2007), but we now and here show it to not be an artifact of spatially averaging over regions with potentially differential motion along the line-of-sight.

In addition, we see that a significant fraction of the bins also show prominent IL (third panel in Figure 2) in the NLIL model. Here, as a preliminary and “pedestrian” indicator, this statement is underpinned by IL-NL flux fractions; the stronger the best-fit IL line the more “significant” it is. However, a more statistically well-defined statement on the need for an IL is based on the models’ Bayesian Evidence and their ratios (“Bayes factors”). We use the leave-one-out cross validation (LOO-CV) method to calculate the evidence (Bailer-Jones, 2012). It is a derivative version of the standard direct numeric integration (marginalization) of the posterior, with the advantage that the prior enters the result only to second order. Figure 3 shows the example where the NLIL model is favoured, for which we get that the logarithmic evidence ratio of the NLIL relative to the NL model is about 1 dex. This means
Figure 3: The top-right blue panel shows the spectrum of one of the bins (solid-black line), the background model (dashed-black line) and components of the intrinsic “best-fit” model (dashed-red lines). The “best-fit” model is overplotted with the solid red line. The remaining 8 panels are 1D-marginalized posteriors over model parameters (solid-black lines): total intrinsic flux, flux fractions in the continuum and lines, NL centroid, IL offset from the NL centroid, and line widths. Dashed-black lines are prior distributions and vertical red lines are the estimated parameters of the “best-fit” model, i.e. the parameters at the maximum of the posterior distribution.

that an IL in addition to a single NL explains our data 10 times better than a simple NL model, irrespective of any particular parameter values – notably, also not only considering the respective best-fit parameters. The logarithmic evidence ratio of the NLIL relative to the NL model for other Voronoi bins is shown in the Figure 2.

In Figure 4 we summarize our results for all Voronoi bins and all the models regardless of the favoured ones. We plot histograms of the best-fit intrinsic NL widths in the NL model, NL widths and their centroid separation in 2NL(IL) and NLNL(IL) models, IL flux fractions, widths and their offsets from the NL centroids. For each of the estimated parameter we also calculate central 95%-confidence interval. The vertical blue-dashed lines show the mean of the 2.5% (left line) and 97.5% (right line) quantile distributions. We often find NL widths being much larger than 20 km s$^{-1}$: $\approx 60$ km s$^{-1}$ is the mean of the NL width in single-NL models; even in the 2NL(IL) and NLNL(IL) models, it is generally $\approx 40$ km s$^{-1}$. The intrinsic IL widths are $\approx 180$ km s$^{-1}$ on average with 30% flux contribution to the total intrinsic flux.

4 Summary

We presented the narrow H$\alpha$ spectroscopic observations of Tycho’s NE Balmer filaments. This study provides spectroscopic data that is for the first time spatially resolved
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Figure 4: Summarized results for all Voronoi bins. Top panels: “best-fit” intrinsic NL widths in NL model, NL widths in 2NL(IL) and NLNL(IL) models, NL centroid separation in all double-NL models. Bottom panels: IL flux fractions, IL widths, IL offsets from the NL centroid in all IL models. Vertical dashed-blue lines show the mean of the 2.5% (left line) and 97.5% (right line) quantile distributions.

(spectro-imagery), with large coverage that comprises and resolves the entire NE filament. Our analysis includes Bayesian model comparison that enables a quantitative, probabilistic and well-defined model comparison. We find that the broadening of the NL beyond $20\,\text{km\,s}^{-1}$ that was noted in previous studies was not an artifact of the spatial integration, and that it extends across the whole filament, not only the previously covered 'knot g'. Likewise, we confirm the suspected presence of an IL, and show it to be widespread. The first result points toward the evidence of heating in the CR precursor, while the second result reveals the presence of the broad-neutral precursor.

Acknowledgments

We would like to thank Coryn Bailer-Jones (MPIA) for useful discussion on Bayesian statistics and Giovanni Morlino (INFN Gran Sasso Science Institute) for discussion on theoretical predictions for the shock emission in Tycho’s SNR.

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