LENS MODEL AND TIME DELAY PREDICTIONS FOR THE SEXTUPLY LENSED QUASAR SDSS J2222+2745*

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Received 2016 September 30; revised 2016 November 20; accepted 2016 December 1; published 2017 January 16

ABSTRACT

SDSS J2222+2745 is a galaxy cluster at z = 0.49, strongly lensing a quasar at z = 2.805 into six widely separated images. In recent Hubble Space Telescope imaging of the field, we identify additional multiply lensed galaxies and confirm the sixth quasar image that was identified by Dahle et al. We used the Gemini-North telescope to measure a spectroscopic redshift of z = 4.56 of one of the lensed galaxies. These data are used to refine the lens model of SDSS J2222+2745, compute the time delay and magnifications of the lensed quasar images, and reconstruct the source image of the quasar host and a lensed galaxy at z = 2.3. This galaxy also appears in absorption in our Gemini spectra of the lensed quasar, at a projected distance of 34 kpc. Our model is in agreement with the recent time delay measurements of Dahle et al., who found τ_{AB} = 47.7 ± 6.0 days and τ_{AC} = −722 ± 24 days. We use the observed time delays to further constrain the model, and find that the model-predicted time delays of the three faint images of the quasar are τ_{AD} = 502 ± 68 days, τ_{AE} = 611 ± 75 days, and τ_{AF} = 415 ± 72 days. We have initiated a follow-up campaign to measure these time delays with Gemini North. Finally, we present initial results from an X-ray monitoring program with Swift, indicating the presence of hard X-ray emission from the lensed quasar, as well as extended X-ray emission from the cluster itself, which is consistent with the lensing mass measurement and the cluster velocity dispersion.

Key words: galaxies: clusters: general – galaxies: clusters: individual (SDSS J2222+2745) – gravitational lensing: strong

1. INTRODUCTION

The rare chance alignment of a quasar behind a strong-lensing cluster provides unique opportunities for studies of different astrophysical objects. Through careful lens modeling, these systems can probe the mass distribution of the foreground lens; the high magnification enhances our ability to study the background quasar, and galaxies between us and the quasar can be seen in absorption along multiple lines of sight in the light of the background quasar. Lensing configurations that involve a quasar lensed by a single massive galaxy are more common; however, the lensing magnification of a single galaxy is typically significantly lower than in the Galaxy cluster case. Unique to the cluster-lensed quasar configurations, the multiple images of the lensed quasar have large separations (14″.6–22″.5; Inada et al. 2003, 2006; Dahle et al. 2013) and high magnifications; the lensed active nucleus is point-like, providing accurate positional constraints, and is variable—enabling measurements of the time delay between images of the same source. The high tangential magnification stretches the host galaxy of the quasar into a giant arc, thus resolving it from the light of the active nucleus, which usually dominates in a high-redshift quasar.

To date, only three cases of high-redshift quasars strongly lensed by a galaxy cluster have been published: SDSS J1004+4112 (Inada et al. 2003), SDSS J1029+2623 (Inada et al. 2006), and SDSS J2222+2745 (Dahle et al. 2013).

SDSS J2222+2745 was discovered as part of the Sloan Giant Arcs Survey (SGAS; Hennawi et al. 2008; Bayliss et al. 2011a, 2011b; Sharon et al. 2014; M.D. Gladders et al. 2017, in preparation). SGAS is a systematic survey of highly magnified lensed galaxies, also referred to as “giant arcs,” in the imaging data of the Sloan Digital Sky Survey (SDSS; York et al. 2000). The lensing identification process starts with optical selection of galaxy clusters from the SDSS photometry catalogs using the cluster red sequence algorithm of Gladders & Yee (2000). Sections of the imaging data around each cluster were then retrieved and processed to generate color images, with scaling parameters selected to optimize the visibility of possible lensing features. The images were visually inspected and ranked for lensing evidence by several observers in a process that enables a calculation of the selection statistics (the process will be described in full in M.D. Gladders et al. 2017, in preparation). All candidates were followed up for confirmation, and the survey purity and completeness were quantified. Bayliss et al.
that is seen embedded in the A1 arc is a foreground white dwarf star (quasar at Figure 1. Color-composite image of SDSS J2222+2745)

In addition, we measured the spectroscopic redshifts of several cluster-member galaxies and of the lensed galaxy A1 at \( z = 2.3 \). Stark et al. (2013) also measure the spectra of the quasar at \( z = 2.807 \), and of the galaxy A1. Interestingly, the spectrum of the quasar shows strong Ly\( \alpha \) absorption at the redshift of the foreground lensed galaxy, as well as Si\( \text{II} \) \( \lambda 1526 \) and C\( \text{IV} \) \( \lambda 1549 \) (Stark et al. 2013), indicating the presence of neutral hydrogen and metals associated with gas surrounding the Galaxy. Stark et al. (2013) estimated that the projected distance between quasar image A and the interloper galaxy A1 is \( \sim 50 \) kpc. We refine this estimate in Section 4.5. Following the discovery of SDSS J2222+2745, we have initiated an imaging monitoring program with the NOT to measure the time delays between the images of the quasar. The results from the first three years of ongoing photometric monitoring with the NOT and the first season of Gemini monitoring are presented in Dahle et al. (2015). The light curves of the three brighter images of SDSS J2222+2745 are measured from an analysis of 42 distinct epochs, resulting in time delays of \( \tau_{\text{AB}} = 47.7 \pm 6.0 \) days and \( \tau_{\text{AC}} = -722 \pm 24 \) days. A robust measurement of the time delays of images D, E, and F requires deeper observations; a monitoring campaign with Gemini was initiated in 2015 (GN-2016A-Q-28; PI: Gladders) for this purpose.

This paper is structured as follows. In Section 2 we describe the HST imaging data of SDSS J2222+2745, Gemini (2011a, 2011b) give the results of the initial spectroscopic follow-up campaign and measure the redshift distribution of the lensed galaxies.

SDSS J2222+2745 was detected in the SGAS search in SDSS Data Release 8 (Aihara et al. 2011) owing to a prominent giant arc that appears 8.5 south of the brightest cluster galaxy. A further investigation of the field revealed the multiply imaged lensed quasar. The field was followed up by Dahle et al. (2013) using the Mosaic Camera (MOSCA) and the Andalusia Faint Object Spectrograph and Camera (ALFOSC) at the 2.56 m Nordic Optical Telescope (NOT).

We have recently obtained Hubble Space Telescope (HST) imaging data of this target (Figure 1; Section 2). As can be seen in Figure 1, a background quasar is lensed by SDSS J2222+2745, forming six images around the core of a galaxy cluster at \( z = 0.49 \). Three bright images appear north of the cluster core (labeled A, B, C; our labeling scheme follows Dahle et al. 2015), and three faint images (D, E, F) can be seen near the central cluster galaxies (G2, G3, G1, respectively). The cluster also lenses other background galaxies, the most prominent of which is seen as a blue arc south of the cluster core (labeled A1 in Figure 1), Dahle et al. (2013) reported on the discovery of SDSS J2222+2745, confirmed the lensing interpretation, presented spectroscopic identification of the lensed quasar, spectroscopic confirmation of the six lensed images of the quasar, and measured its redshift to be \( z = 2.82 \).

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spectroscopy, and Swift X-ray observations. We present a new strong-lensing analysis based on the new data in Section 3. In Section 4, we present and discuss the predicted time delays, cluster mass, lensing magnification, source reconstruction, and absorbing systems. We conclude with future work in Section 5. Throughout this paper, we assume a flat cosmology with $\Omega_M = 0.7$, $\Omega_{\Lambda} = 0.3$, and $H_0 = 70$ km $s^{-1}$ Mpc$^{-1}$. In this cosmology, 1” corresponds to 6.0384 kpc at the cluster redshift, $z = 0.49$. Magnitudes are reported in the AB system.

2. DATA

2.1. HST Imaging

SDSS J2222+2745 was observed by HST Cycle 21 program GO-13337 (PI: Sharon) with WFC3 F160W for 1311 s and F110W for 1211 s on 2014 August 10, and with ACS F435W, F606W, and F814W for 4944 s each on 2014 October 10–11. The filters were carefully selected to provide the best sensitivity to the different sources in the field. The bluest filter, F435W, is sensitive to emission from the quasar and its host, and gives a high contrast between the quasar and the cluster galaxies, as can be seen in Figure 2. At $z = 0.49$ most of the light from typical elliptical galaxies is redshifted to wavelengths longer than the ACS/F435W response curve, and we expect to see little emission in this band from the cluster galaxies. ACS/F606W and ACS/F814W give good sampling of the spectral energy distribution of typical early-type cluster galaxies, and the reddest filters help detect lensed high-$z$ dropout galaxies and provide a long wavelength baseline for galaxy colors and SED fitting.

Each of the ACS images was taken over two orbits, with three gap-crossing subpixel dither positions in each orbit (a total of six subexposures) for better sampling of the point-spread function, removal of cosmic rays and hot or bad pixels, and to cover the chip gaps. A half field of view offset was implemented between the two orbits of observation in each filter. Since the strong-lensing regime is small enough to fit within one ACS chip, this design ensures that the center of the field is imaged to the full depth of two orbits per filter, which is needed to obtain the required signal-to-noise ratio (S/N), while at the outskirts we allowed shallower exposure. The increased field of view enables studies that require high resolution at somewhat larger cluster-centric radii, including weak lensing measurements, selection of cluster-member galaxies for strong-lensing analysis, and galaxy cluster science.

The WFC3-IR observations were executed within a single orbit, four images per filter with small box dithers for PSF reconstruction and to cover artifacts such as the “IR Blobs” and “Death Star” (WFC3 Data Handbook; Rajan et al. 2011). We used the sampling interval parameter SPARS25.

The subexposures of each filter were reduced and combined following the reduction pipeline of our Cycle-20 program GO-13003 (e.g., Sharon et al. 2014). The WFC3-IR images were treated using a custom algorithm to remove the “IR Blobs”, and we corrected the ACS images for CTE losses prior to drizzling. Individual corrected images were combined using the Astro-Drizzle package (Gonzaga et al. 2012) with a pixel scale of 0.030 pixel$^{-1}$ and a drop size of 0.5 for the IR filters and 0.8 for the ACS filters. This approach provides good recovery of the PSF in all bands and maximizes the sensitivity to detail. All images were aligned onto the same pixel frame. In the final reduced data, the 5$\sigma$ limiting magnitudes in the five filters are 27.4, 27.8, 27.3, 26.8, and 26.5 mag within a circular aperture of diameter 0″7, for F435W, F606W, F814W, F110W, and F160W, respectively.

A photometric catalog of all the objects in the overlapping ACS and WFC3 field of view was generated following procedures outlined in Skelton et al. (2014), and spectral energy distribution (SED) fits and photometric redshifts were derived using EAZY (Brammer et al. 2008). We note that the fidelity of the photometric redshift is limited by the small number of filters; nevertheless, the photometric redshifts are found to be consistent with the available spectroscopic redshifts.

2.2. Gemini Spectroscopy

The main scientific goal of the HST observations was to facilitate a detailed lens model of SDSS J2222+2745. Strong lens modeling relies on constraints from observational evidence of strong lensing, in the form of multiple images of lensed background sources. The positions and redshifts are used as local solutions of the lensing equations to constrain the projected mass density distribution at the core of the cluster. The accuracy of a lens model strongly depends on the availability of lensing constraints. The mass distribution and lensing magnification are sensitive not only to the accurate identifications and positions of multiple images, but also to the redshifts of these lensed galaxies. This is especially important when there are few lensed sources identified (Johnson & Sharon 2016). Lens models that are computed with no spectroscopic redshifts as constraints are shown to produce erroneous results (e.g., Smith et al. 2009; Johnson & Sharon 2016); it is therefore critical to include constraints from at least a few spectroscopically confirmed source redshifts.

We were awarded 4.5 hr of Band One queue observations with Gemini Multi-Object Spectrograph (GMOS; Hook et al. 2004) on the Gemini-North telescope (GN-2015B-Q-27; PI: Sharon) to secure spectroscopic redshifts of the secondary arcs that were identified in the new HST data.

Observations of this program were executed on UT 2015 September 10 and 2015 November 6 and 7. Conditions at the times of observation were photometric, with seeing between

Figure 2. Response function of the five filters that were used in the HST observation (GO-13003; PI: Sharon) overplotted on a template spectrum of an elliptical galaxy, redshifted to the cluster redshift, $z = 0.49$ (black), and a template quasar spectrum redshifted to the quasar redshift, $z = 2.053$ (gray). The filters sample the spectral energy distribution of cluster galaxies as well as the quasar and its host, and provide good contrast between these sources. The broad wavelength coverage supports SED fitting and identification of secondary arcs. Bottom: spectra of images A, B, and C of the quasar from Dahle et al. (2013).
0\arcsec.5–0\arcsec.85. The field was imaged by our NOT/ALFOSC monitoring program during the same dark runs, indicating little variability between these epochs; we report the g-band photometry for reference: on 2015 September 13.16, g(A) = 21.67; g(B) = 22.07; g(C) = 21.76. On 2015 November 07.90, g(A) = 21.71 mag; g(B) = 21.98 mag; g(C) = 21.52 mag. For the Gemini/GMOS observations, GMOS was configured in macro nod-and-shuffle (N&S) mode with the R400_G5305 grating in first order and the G515_G0306 long pass filter. The detector was binned by a factor of 2 in the spectral direction and unbinned spatially. Following extensive previous experience using GMOS in this mode (e.g., Bayliss et al. 2011b, 2014), we chose an N&S cycle length of 120 s as a balance between achieving good sampling of time variation in the sky and limiting charge trap effects by minimizing the number of shuffles in a given integration.

We designed two multi-object slit masks that preferentially placed slits on faint candidate strongly lensed background sources around the core of SDSS J2222+2745 (see Figure 3 for mask design and Figure 1 for source IDs). Mask 1, at the position angle of 65\degree, targeted lensing candidate images B1, B2, B3, C2, D1, D3, and a faint edge of A1; image C of the quasar; and image A of the host galaxy of the quasar. Mask 2 at the position angle of 47\degree targeted arcs A1, B1, C3, and D2 and quasar images A, B, C, and D. Both masks targeted cluster-member galaxies and other galaxies in the field.

Slits were placed so as to target high-priority sources at both the original pointing position and the offset nod position; this slit strategy is the same as described in Bayliss et al. (2011b), and we refer to that paper for a detailed description. Most slits on each mask were 1\arcsec wide, with lengths varying from slit to slit. Two slits on each mask had widths of 0.5\arcsec; these were placed on the three brightest red galaxies in the core of the cluster to produce higher resolution spectra, which may potentially inform stellar velocity dispersion measurements for those galaxies. Each spectroscopic mask was exposed twice for 2400 s, with a wavelength dither between the exposures to cover the chip gaps in the GMOS detector array.

We reduced the resulting GMOS spectra using a suite of custom tools that was developed using the XIDL\textsuperscript{13} package; this pipeline is similar to that used in Bayliss et al. (2014). For N&S spectra, sky subtraction simply requires differencing the two shuffled sections of the detector. We first performed this differencing of the raw spectra, and then wavelength-calibrated, extracted, stacked, and flux-normalized spectra from each slit on each of the two masks. Flux calibration was performed using an archival standard star. The archival calibration provides a reliable relative flux correction, but does not yield an absolute flux calibration. The spectral resolution of the final data is \( R \approx 700–1100 \) (270–430 km s\(^{-1}\)) for spectra taken through 1\arcsec wide slits, and \( R \approx 1400–2200 \) (135–215 km s\(^{-1}\)) for spectra taken through 0\arcsec.5 wide slits.

We summarize the results of the Gemini spectroscopy observations in Table 1. Details of the spectroscopic analysis of the high-priority sources are given below.

Quasar images: we refine the redshift measurement of the quasar, and obtain \( z = 2.8050 \pm 0.0006 \) from the spectra of images A, B, and C of the quasar (Figure 4, top panel). We observe emission lines from He II 1640, O III 1666, [O II] 2470, and C II 3237, and C IV 1549. We also detect absorption lines from Mg II and other elements at \( z = 2.296 \) from the intervening galaxy A1 (see Section 4.5). The spectrum of image D is dominated by light from the foreground cluster galaxy; however, C IV and C III emission lines from the quasar can be detected. A slit targeting the host galaxy of image A of the quasar (see Figure 3 for slit placement) resulted in a low S/N spectrum that is dominated by light from the nucleus.

Lensed galaxy A1: from two slitlets in Mask 2, we confirm the known arc redshift of \( z = 2.3 \) from ISM absorption lines Fe II 2344, 2382; Fe II 2586, 2600; and Mg II 2798, 2803. We identify weak nebular emission of Si II\textsuperscript{15} 1892 and C III\textsuperscript{16} 1909. The combined spectrum is shown in Figure 4. The slit that targeted the faint region of the arc did not result in sufficient S/N.

Lensed galaxy B: Figure 4 shows stacked spectra of arc B1 from four slitlets, two in Mask 1 and two in Mask 2. We identify emission lines from Ly\alpha, Si II 1260, O I–Si II 1303, He II 1640, and C IV 1449 at \( z = 4.56 \). The images of B drop out completely from the ACS/F435W filter, which supports this redshift interpretation. Furthermore, the photometric redshift analysis obtained for this source from the five HST bands shows a single high-significance peak around \( z_{\text{phot}} = 4.4 \). The slits placed on B2 and B3 resulted in too low S/N for an independent measurement of the redshift. Nonetheless, we detect a faint emission line in these spectra that is consistent with Ly\alpha at the same redshift as image B1.

Lensed galaxy C: we targeted C2 and C3, with a total on-target exposure time of 2400 s on each image; however, since these sources are faint, the resulting spectra have low S/N. A possible absorption line is detected at 6210 Å. Interpreting this absorption feature as the C IV 1548,1550 lines, which are often among the most prominent rest-frame UV features in star-forming galaxies, places this source at \( z = 3.01 \). We note that this putative spectroscopic redshift is also consistent with the photometric redshift analysis and favored by the lensing analysis. Nevertheless, given its low certainty, we do not

\textsuperscript{13} http://www.ucolick.org/~xavier/IDL/index.html

Figure 3. Sources that were targeted for Gemini-North GMOS multislit spectroscopy are labeled in green (Mask 1) and red (Mask 2). Faint sources were targeted by both masks or in both nod positions, in order to maximize their signal-to-noise ratio.
consider this a secure spectroscopic redshift for the purpose of lensing analysis.

Lensed galaxy D: we placed slits on D1, D2, and D3. As can be seen in Figure 3, the slits are expected to contain light from adjacent sources (in particular, blue emission from a nearby galaxy). The spectroscopic analysis results in a low confidence redshift of $z = 0.837$ for D1 and D2, based on Cα and K lines, and no signal in D3. The photometric redshift probability distribution function is bimodal, with a high-significance peak around $z = 4.4$ and low-significance peak around $z = 0.74$ for images D1 and D3. Image D2 shows only one peak at $z = 0.74$. Since this is the image that is most contaminated by blue light from the nearby galaxy, we argue that this interpretation is consistent with two separate redshifts for two different background sources: a blue arc at low $z$, consistent with the possible $z = 0.837$ that is suggested by the spectroscopy, and a high-redshift source at $z \sim 4.4$, which is likely the three-imaged lensed source D. Due to the ambiguous redshift interpretation, we leave this redshift as a free parameter as well, with the upper redshift prior $z < 5$ set by the photometric redshift analysis.

Cluster galaxies: we measure spectroscopic redshifts of 11 cluster galaxies, including the central galaxies G1, G2, G3, and G4. These measurements confirm the published spectroscopic redshifts of G1, G2, and G3 from the NOT (Dahle et al. 2013). In the spectrum of galaxy G3 we detect weak C IV emission at...
Figure 4. Gemini/GMOS spectra of the quasar and arcs A, B, C, and D in SDSS J2222+2745. The noise level is plotted in magenta. Emission and absorption lines are noted. In blue, we overplot the composite stacked spectra of Lyman Break Galaxies from Shapley et al. (2003).
$z = 2.805$ from the embedded quasar image E. In Table 1 we also list the redshifts of three galaxies with SDSS-DR9 spectroscopy that are within a projected radius of 1500 $h^{-1}$ kpc from the BCG. From these 14 members we measure a cluster redshift of $z = 0.4897 \pm 0.0032$ and a velocity dispersion of $\sigma_v = 657 \pm 166 \text{ km s}^{-1}$ using the Gapper estimator (Beers et al. 1990). The uncertainties on the velocity dispersion are calculated as $\pm 0.91\sigma_v / \sqrt{n-1}$, where $n$ is the number of galaxies, following Ruel et al. (2014). Using the mass scaling relation in Evrard et al. (2008), the velocity dispersion translates to a dynamical mass of $M_{200, \text{dynamical}} = 3.9_{-2.8}^{+3.6} \times 10^{15} M_\odot$.

Other galaxies: Table 1 also lists the coordinates and the spectroscopic redshifts of other background (i.e., behind the cluster) and foreground galaxies in the field that were measured from these data.

### 2.3. Swift X-Ray Observations

SDSS J2222+2745 was observed at X-ray wavelengths by the Swift X-ray telescope (XRT) as part of a monitoring program using University of Michigan time (PI: Sharon). Observations were taken approximately every six weeks over seven epochs between 2015 September 16 and 2016 June 29, with a combined exposure time of 90.5 ks. The typical exposure time was 15 ks per epoch, with the exception of epoch 1, which was observed for $\sim$10 ks (see Table 2). The hard X-ray radiation ($>3 \text{ keV}$) varies during this time by up to a factor of three between epochs with the lowest and the highest counts per second, confirming the variable nature of the quasar at these wavelengths. However, the Swift XRT resolution (see below) is not sufficient to robustly resolve the three brightest images of the lensed quasar. A decomposition analysis of the variable emission is beyond the scope of this paper and will be presented in future work. Here, we present the co-added data from the first seven epochs, and analyze the X-ray emission from the cluster hot gas.

The data were reprocessed using HEASOFT v. 6.17 and the most up-to-date version of CALDB, accessible via remote server. New Level 2 event files were created using the tool xrtpipeline. We used the XRT Data Product Generator to combine images from different epochs, and for astrometric measurements. We verified the absolute astrometric solution by matching the coordinates of a bright X-ray star at [R.A., Dec.] = [335.39729, 27.707253], with its optical counterpart from the SDSS.

![Figure 5. Three-color HST image of SDSS J2222 with Swift X-ray contours overlaid in green and the lensing mass contours in white. The red ellipse indicates the statistical uncertainty on the centroid of the main cluster-halo component from the lensing analysis (see Section 3 and Table 3). The X-ray emission was smoothed with a Gaussian kernel matching the Swift PSF. Contours are linearly spaced. The thick, horizontal green bar in the upper left-hand corner of the image is $3''$ in length, which is the size of the astrometric uncertainty.](image)

The Swift XRT has a PSF of 18'' at 1.5 keV; at this resolution, the X-ray radiation from the images of the lensed quasar is blended with the diffuse emission from the hot cluster X-ray gas. Nevertheless, their contribution is wavelength dependent, with the soft X-ray radiation ($\lesssim 3 \text{ keV}$) dominated by the cluster emission, and the hard X-ray photons attributable to the quasar. In order to separate the cluster emission from the quasar emission, we co-add the emission in the 0.3–3.0 keV range from all seven epochs. The resulting X-ray contours are overlapped on the optical image in Figure 5. We find that the soft X-ray emission is centered on [R.A., Decl.] = [335.53613, 27.760667], with a 90% confidence error radius of 3'' (see Evans et al. 2014 for more information on the way the astrometric position is determined). This position is in excellent agreement with the center of the main cluster-halo component as derived from the lensing analysis (Section 3). The two centroids are 1''11 in projection, a distance which is within the 3'' XRT astrometric uncertainty. Nevertheless, since the XRT Data Product Generator is not optimized for measurements of extended sources, the uncertainty may be underestimated.

For an estimate of the cluster mass, we measure the background-subtracted X-ray flux from the co-added data of the seven epochs, in the energy range 0.1–2.4 keV, within an aperture of radius 1 Mpc centered on the cluster; we assume that this radius corresponds roughly to $R_{200}$ (e.g., Mantz et al. 2010), and that in this energy range the X-ray radiation is dominated by the cluster with negligible contamination from the background quasar. To account for errors due to the unknown gas temperature, we consider a range of gas temperatures between $kT = [3.06-9.67]$ keV, and find luminosities in the range $L_x = [1.0-1.4] \times 10^{44}$ erg s$^{-1}$. The luminosity is within the range expected for clusters with similar velocity dispersion (Xue & Wu 2000). We use the Mantz et al. (2010) $M-L_X$ relation to estimate the cluster mass.

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Table 2: Swift Observation Information

| OBSID     | Start Date | Exp. Time (ks) | Epoch |
|-----------|------------|----------------|-------|
| 00034046001 | 2015 Sep 16 | 2.4          | 1     |
| 00034046002 | 2015 Sep 27 | 6.2          | 1     |
| 00034046003 | 2015 Nov 06 | 12.8         | 2     |
| 00034046004 | 2015 Dec 18 | 9.0          | 3     |
| 00034046005 | 2015 Dec 20 | 3.8          | 3     |
| 00034046006 | 2016 Jan 30 | 13.7         | 4     |
| 00034046007 | 2016 Apr 13 | 15.6         | 5     |
| 00034046008 | 2016 May 16 | 14.1         | 6     |
| 00034046009 | 2016 Jun 28 | 3.3          | 7     |
| 00034046010 | 2016 Jun 29 | 9.5          | 7     |

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14 http://www.swift.ac.uk/user_objects/index.php
\[ M_{500, x} = [0.94 - 1.2] \times 10^{14} M_{\odot}. \] The X-ray-inferred mass estimate is in line with the lensing mass measurement and with the dynamical mass. A more robust measurement of the X-ray mass will be enabled with higher resolution Chandra data, with which the emission from the cluster gas and the background quasar can be spatially disentangled.

3. STRONG-LENSING ANALYSIS

3.1. Multiple Images and Lensing Constraints

The lens model of SDSS J2222+2745 relies on observational strong-lensing evidence, in the form of multiply imaged galaxies. The multiband HST images are uniquely useful for the task, owing to their high resolution and broad wavelength coverage that allow multiple images of individual background sources to be identified by their color and morphology. In Dahle et al. (2013) we identified six images of one background quasar in imaging data from the NOT. We confirmed five of these images and secured their redshift through spectroscopy. The sixth image was predicted by the preliminary lens model and identified in the data after modeling and subtracting the light of the cluster galaxies at the core of the cluster; Dahle et al. (2013) provide strong evidence for the presence of the sixth image. The HST images confirm the sixth image as a counterimage of the quasar, with a point-like PSF and colors similar to the other quasar images. These images are labeled A, B, C, D, E, and F in Figure 1. A lensed galaxy A1, at \( z = 2.3 \) (Dahle et al. 2013; Stark et al. 2013), is distorted by the cluster and appears as a blue giant arc south of the cluster center. The new HST data reveal substructure in the giant arc A1, but do not lead to an identification of a counterimage of this galaxy. We interpret this giant arc as a likely result of source-plane caustics that bisect the Galaxy or pass very close to it, resulting in high magnification in the tangential direction (see Section 4.4).

We identify three secure strongly lensed galaxies with multiple images in the new HST data.

Source B has three multiple images with unique colors, morphological resemblance, and the expected parity. We measure a spectroscopic redshift of \( z_{B, \text{spec}} = 4.56 \) using GMOS on Gemini North (see Section 2.2).

Source C is a faint source observed as three images with lensing configuration similar to the three brighter quasar images north of the cluster core. Due to the low surface brightness of C1, C2, and C3, we were not able to obtain a secure spectroscopic redshift. The photometric redshift, spectroscopy, and lensing geometry are all consistent with it being at \( z_{C, \text{phot}} \sim 3 \) (see Section 2.2). We leave the redshift of this source as a free parameter in the lensing analysis, with broad priors based on the photometric redshift analysis, \( 2.0 \leq z_c \leq 4.0 \). We expect that further counterimages of this source would be too faint and embedded in the light of the bright cluster galaxies to be detected in the existing data.

Three images of source D appear in the WFC3/IR bands, south of a cluster-member galaxy in the south part of the cluster core. As described in Section 2.2, we were unable to measure a secure spectroscopic redshift for this source. We leave the redshift of this source as a free parameter in the lensing analysis, with broad priors based on the photometric redshift analysis, \( 3.8 \leq z_D \leq 5.0 \).

We identify other candidates of lensed galaxies; however, these are not robustly confirmed as strong-lensing features and thus are not used as constraints in the lens model.

We use the positions of the six quasar images, arcs A1, B1-3, C1-3, and D1-3 to constrain the lens model. Resolved emission knots and substructure in the host galaxy of the quasar and B1-3 are also used as additional positional constraints. The redshifts of the quasar and sources C and D are left as free parameters, with broad priors set by the probability distribution functions of their photometric redshifts.

3.2. Strong Lens Model

The lens model is computed using the public software Lenstool (Jullo et al. 2007). Lenstool relies on a “parametric” modeling algorithm, in which the mass distribution is assumed to be a combination of a number of halos, each described by a set of parameters. The software uses the Markov Chain Monte Carlo (MCMC) procedure to sample the parameter space, determine the best set of parameters that minimize the scatter between the observed and predicted positions of multiply imaged lensed galaxies, and determine their uncertainties.

SDSS J2222+2745 is modeled with one cluster-scale halo, plus galaxy-scale halos. Each of these halos is modeled as a Pseudo-Isothermal Elliptical Mass Distribution (PIEMD; also known as a dual Pseudo Isothermal Elliptical Mass Distribution; Ellasdóttir et al. 2007). The parameters of this mass distribution are positions \( x \) and \( y \), ellipticity, \( e = (a^2 - b^2)/(a^2 + b^2) \), where \( a \) and \( b \) are the semimajor and semiminor axes, respectively; position angle \( \theta \), measured north of west; core radius \( r_{\text{core}} \); cut radius \( r_{\text{cut}} \); and effective velocity dispersion \( \sigma_0 \). We allow all the parameters of the cluster-scale halos to vary, except for \( r_{\text{cut}} \), which, for a typical cluster, is much larger than the radius in which lensing evidence can be found and thus cannot be constrained by the model. We fix the cluster-halo \( r_{\text{cut}} \) at 1500 kpc.

Cluster-member galaxies are selected from a color–magnitude diagram, as those with colors that place them on the cluster red sequence (Gladders & Yee 2000). We note that some galaxies at this redshift may not be quiescent and therefore fall off this relation. However, they are not a dominant component at the core of the cluster (e.g., Fairley et al. 2002). The cluster galaxies are also modeled as PIEMDs, with the morphological parameters \( (x, y, PA, \theta) \) fixed to their observed values as measured from the HST data in ACS/F814W. \( r_{\text{core}}, r_{\text{cut}}, \) and \( \sigma_0 \) are assumed to correlate with the luminosity of each galaxy (see Limousin et al. 2005 for a description of the scaling relations).

The slope parameters of five galaxies at the center of the cluster are allowed to deviate from the scaling relation. The lensing potential of the three brightest galaxies near the core of the cluster is responsible for the appearance of the three fainter images of the quasar—D, E, and F. In a close inspection of the galaxies near images D and F, we find that the peak of the surface brightness is not aligned with the center of the light distribution of these galaxies, implying a more complex projected mass distribution than that of a single elliptical halo, at least of its stellar mass component. This may be due to the merger history of these galaxies (e.g., Lidman et al. 2013; Lavoie et al. 2016) or a projection effect. We therefore model each of these galaxies as a combination of two halos. One halo has its \( x, y \) parameters fixed to the center of the extended light distribution of the Galaxy, its ellipticity and position angle follow those of the light distribution, and the other parameters
allowed to vary. The second halo is centered on the peak surface brightness, with circular symmetry, vanishing core radius, and $\sigma_0$ and $r_{\text{out}}$ set as free parameters.

The distribution of the intracluster light is observed to be more extended in the north–south direction (Figure 1), which would be consistent with a young dynamical age for the cluster. However, the deep combined NOT and Gemini images (Dahle et al. 2015) indicate considerable Galactic cirrus in the field, which is difficult to disentangle from intracluster light at the very faintest surface brightness levels.

Although we find that some of the free parameters are not sensitive to the positional lensing constraints, we allow these parameters to vary in order to encompass the full range of statistical uncertainties, and investigate their effect on the time delay of the quasar images.

In Table 3, we list the lens model parameters and their uncertainties, including the time delay constraints (95% confidence limit from Dahle et al. 2015). We plot the critical curves from the best-fit model in Figure 6, for a source at $z = 2.805$. The best-fit model has an image-plane rms of 0.016. We note that since the rms was computed from the predicted positions of the same images that were used as constraints, it is not an unbiased indicator of the model fidelity (Johnson & Sharon 2016).

The time delay between the images of the quasar can be measured from the arrival time surface (e.g., Schneider 1985),

$$\tau(\theta, \beta) = \frac{1}{c} \frac{D_I D_S}{D_L} \left( \frac{1}{2} (\theta - \beta)^2 - \psi(\theta) \right),$$  

(1)

where $\beta$ is the source location, $\theta$ is a coordinate in the image plane, $z_l$ is the lens redshift, $D_l$ and $D_s$ are the distances from the observer to the lens and to the source, respectively, $D_{ls}$ is the distance from the lens to the source, and $\psi$ is the lensing potential. Figure 7(a) shows the Fermat potential of the best-fit model, with the positions of the observed quasar images overplotted. Multiple images occur in stationary points in this potential, i.e., maximum, minimum, and saddle points. The lens model successfully predicts the formation of all the observed quasar image as well as three additional demagnified images, each within $0''1$ of the center of galaxies G1, G2, and G3, at the extremum points of the Fermat potential. However, these images are predicted to be several magnitudes fainter than the faintest observed image of the quasar, with 29–34 mag in the F435W band, and thus we do not expect to be able to detect them in the current data.

We report the predicted arrival time in days relative to image A of the quasar, $\Delta t = \tau(\theta, \beta) - \tau(\theta_A, \beta)$. As can be seen in Equation (1), the Fermat potential depends on the source position, $\beta$. It is in fact very sensitive to small changes in the exact value of $\beta$. We therefore follow the procedure described in Sharon & Johnson (2015) and take the source-plane scatter into account when computing the uncertainties of the time delay of the quasar images. The best-fit time delays and their uncertainties are listed in Table 4.

Time delays are not implemented as constraints at this point. We derive a lens model with no prior on the time delays and later confront the model with the measured time delays from Dahle et al. (2015) in a posterior analysis—see Section 4.1. After applying the observational time delay constraints on the posterior distribution, we find that parts of the parameter space are excluded.

Table 3: Best-fit Lens Model Parameters

| No. | Component      | $\Delta$ R.A. ($''$) | $\Delta$ Decl. ($''$) | $e$    | $\theta$ (deg) | $r_{\text{core}}$ (kpc) | $r_{\text{out}}$ (kpc) | $\sigma_0$ (km s$^{-1}$) |
|-----|----------------|----------------------|-----------------------|--------|----------------|--------------------------|-------------------------|--------------------------|
| 1   | Cluster halo   | 0.26 ± 0.22          | 2.53 ± 1.20           | 0.29 ± 0.05 | 95.8 ± 2.1      | 42.7 ± 6.5               | [1500]                  | 668 ± 22                  |
| 2   | G1 halo        | [0.029]              | [0.036]               | [0.062] | [24.5]         | [0.13 ± 0.13]            | 24.9 ± 23.5             | 274 ± 85                  |
| 3   | G1 core        | [0]                  | [0]                   | [0]    | [0]            | [23.6 ± 23.2]            | 30.3 ± 19.5             |
| 4   | G2 halo        | [1.895]              | [−2.351]              | [0.669] | [−15.6]        | 0.15 ± 0.13              | 11.0 ± 8.3              | 294 ± 104                 |
| 5   | G2 core        | [1.895]              | [−2.347]              | [0]    | [0]            | [0.001]                  | 24.9 ± 20.9             | 29.2 ± 18.8               |
| 6   | G3 halo        | [0.583]              | [−5.339]              | [0.222] | [51.1]         | 0.16 ± 0.13              | 27.7 ± 22.3             | 209 ± 25                  |
| 7   | G3 core        | [0.583]              | [−5.339]              | [0]    | [0]            | [0.001]                  | 26.7 ± 22.8             | 32.2 ± 17.5               |
| 8   | G4             | [−4.425]             | [−14.789]             | 0.49 ± 0.20 | −74.7 ± 3.9 | 3.56 ± 1.32              | 18.5 ± 14.6             | 360 ± 129                 |
| 9   | G5             | [3.35]               | [5.605]               | 0.66 ± 0.13 | −60.0 ± 9.7 | [0.043]                  | [7.213]                | 56.2 ± 43.2               |

Note. The coordinates are given in arcseconds measured east and north of the core of galaxy G1, at [R.A., Decl.] = [335.535745, 27.759886]. All the mass components are parameterized as PIEMD, with ellipticity expressed as $e = (a^2 - b^2)/(a^2 + b^2)$, $\theta$ is measured north of west. Error bars are inferred from the MCMC optimization and correspond to 1$\sigma$. Parameters that were not optimized are listed in square brackets. The location and the ellipticity of the matter clumps associated with cluster galaxies were kept fixed according to their light distribution, and the other parameters were determined through scaling relations (see text).
We now confront the lens model with the time delay observations. The basic lensing analysis predicts that the arrival time is shortest for image C of the quasar, followed by images A, B, F, D, and E. Quantitatively, we find $\tau_{AB} = 47 \pm 20$ days and $\tau_{AC} = -726 \pm 294$ days, in good agreement with the observed measurements of Dahle et al. (2015).

Next, we use the observed time constraints and their 95% confidence limits to further constrain the parameter space. We select the sets of parameters from the MCMC sampling that result in lens models with $\chi^2$ in the range $[\chi^2, \chi^2 + 4.5]$. We consider these models as producing reasonable scatter in the predicted versus observed positions of images of the lensed galaxies, and their parameters are drawn from a range larger than the 1σ confidence interval of the parameter space of well-constrained parameters, as sampled by the MCMC process. Models with larger $\chi^2$ were rejected. We then compute the Fermat potential for each of these sets of parameters (Equation (1)), assuming that the quasar source position $\beta$ is at the mean of the predicted source positions of the six quasar images. We compute the excess arrival time relative to image A of the quasar, i.e., the predicted time delay for each of the images. We identify the models that predict time delays $\tau_{AB}$ and $\tau_{AC}$ within the 95% confidence limit of the observed values of Dahle et al. (2015). In Figure 8, we plot the positional $\chi^2$ against each of the parameters of the main cluster halo and color-code the models that predict either $\tau_{AB}$ in the range $47.7 \pm 6.0$ days, $\tau_{AC}$ in the range $-722 \pm 24$ days, or both. As can be seen in Figure 8, while models that predict the observed $\tau_{AB}$ span the entire parameter space, the measured time delay between image C and A, $\tau_{AC}$, has good constraining power over some of the parameters, mainly the overall mass of the main cluster halo ($\sigma_0$), and its ellipticity ($\epsilon$).

We find a strong correlation between the predicted time delays $\tau_{AD}$, $\tau_{AE}$, and $\tau_{AF}$, as can be seen in Figure 9. Interestingly, $\tau_{AD}$, $\tau_{AE}$, and $\tau_{AF}$ do not correlate with $\tau_{AB}$, but

### 4. RESULTS AND DISCUSSION

#### 4.1. Time Delays

Observational measurement of the time delays between the images of the quasar can provide valuable constraints on the lens model, as the arrival time is sensitive to the lensing potential. SDSS J2222+2745 gives us a unique opportunity to obtain observational constraints on the time delay from six images of the same background quasar, three of which appear close to the cluster core, in close proximity to cluster galaxies. In Dahle et al. (2015), we report on the measurement of time delays between the three bright images of the quasar, $\tau_{AB} = 47.7 \pm 6.0$ days and $\tau_{AC} = -722 \pm 24$ days (all the time delays are measured as excess arrival time relative to image A of the quasar). Our basic lensing analysis does not use the time delays as constraints, and is done strictly without any a priori knowledge of the time delays.

#### Table 4

| Image | Magnitude (F435W) | Magnification | Time Delay (days) |
|-------|-------------------|---------------|-------------------|
| A     | 21.861            | 14.5 ± 2.7    | ...              |
| B     | 22.261            | 10.8 ± 4.3    | $\tau_{AB}$ [47.7 ± 6.0] |
| C     | 22.277            | 6.7 ± 1.0     | $\tau_{AC}$ [-722 ± 24] |
| D     | 23.827            | 1.43 ± 0.75   | $\tau_{AD}$ 502 ± 68 |
| E     | 24.070            | 0.76 ± 0.39   | $\tau_{AE}$ 611 ± 75 |
| F     | 24.909            | 0.95 ± 0.65   | $\tau_{AF}$ 415 ± 72 |

Note. Magnitudes in the ACS/F435W filter are measured within an aperture of radius 0.556 in an observation starting on JD 2456941.06751. Time delay is given in days, relative to image A. $\tau_{AB}$ and $\tau_{AC}$ are observational constraints from Dahle et al. (2015). The uncertainties represent the 95% confidence level from the combined MCMC analysis and the observational time delay constraints.
Figure 8. Goodness of fit plotted against the parameter value, for sets of parameters from the MCMC analysis. The goodness of fit is estimated via the $\chi^2$ value, computed by LensTool as the scatter between the observed and predicted image positions. Models that predict $\tau_{AB}$ in the range $47.7 \pm 6.0$ days are plotted in red squares, models that predict $\tau_{AC}$ in the range $-722 \pm 24$ days are plotted in blue circles, and models that satisfy both criteria are circled in black. All other models are plotted in gray circles. The observed time delay $\tau_{AC}$ has constraining power over the parameters of the main cluster halo (see panels of #01), mainly the normalization $\sigma_0$, which is correlated with the overall mass of the cluster, and the ellipticity $e$.

Figure 9. Correlations between the predicted relative time delays of the six quasars. The top and bottom rows show $\tau_{AB}$ and $\tau_{AD}$ respectively, plotted against the other relative time delays. Colors and symbols are the same as in Figure 8. We see a correlation among all the relative time delays except for $\tau_{AB}$. Thus, the observational measurements of $\tau_{AB}$ and $\tau_{AC}$ (Dahle et al. 2015) have strong constraining power over the model. Furthermore, observational measurement of any of the A–D, E, and F time delays will narrow the uncertainty on the predicted time delays of the other images.
they have strong correlation with \( \tau_{AC} \). This correlation places a tight constraint on the predicted time delays of the three central images. Moreover, the arrival times of images D, E, and F are strongly correlated, which means that a time delay measurement for one of them will provide an additional strict constraint on the time delays of the other images.

The correlation of the time delays of the central images is not surprising. The arrival time lag of the central images is dominated by gravitational time delay as the light travels closer to the center of mass, due to the deep potential well of the cluster; light will take longer to travel on this path, although this path is geometrically shorter (with smaller impact parameter and smaller deflection). Thus, \( \tau_{AC} \) is linked to \( \tau_{AD} \), \( \tau_{AE} \), and \( \tau_{AF} \) through its correlation with the overall normalization of the cluster halo, i.e., the effective velocity dispersion, \( \sigma_v \).

Applying the time delay observational cut on the parameter space, we are able to narrow down the uncertainties on the predicted time delays of the central images. Interestingly, we find that these time delays are short enough to be measured within the next few years: \( \tau_{AD} = 502 \pm 68 \), \( \tau_{AE} = 611 \pm 75 \), and \( \tau_{AF} = 415 \pm 72 \). Moreover, the arrival time of E and F relative to D is short—of order 3–5 months: \( \tau_{DE} = 102 \pm 23 \) and \( \tau_{DF} = -85 \pm 39 \) days, thus measuring \( \tau_{DE} \) and \( \tau_{DF} \) can be achieved within a year or two of cadenced imaging with a large telescope (Section 5).

In the following sections, the results of the lensing analysis take into account the constraints from the observed time delays, as measured by Dahle et al. (2015), and their 95% confidence interval as described above.

4.2. Cluster Mass

We report the lensing-inferred total projected mass density of the lens (cylindrical mass) within projected radii of 100, 200, and 500 pc: \( M(<100\text{ kpc}) = 0.55 \pm 0.03 \times 10^{14} M_{\odot} \), \( M(<200\text{ kpc}) = 1.15 \pm 0.1 \times 10^{14} M_{\odot} \), and \( M(<500\text{ kpc}) = 2.50 \pm 0.24 \times 10^{14} M_{\odot} \pm 10\% \) systematic uncertainty. The statistical uncertainties are derived from the MCMC sampling of the parameter space, combined with the Dahle et al. (2015) 95% confidence interval of the time delay measurements (see Section 4.1). An additional 10% systematic uncertainty should be applied, given the relatively small number of constraints and spectroscopic redshifts, which limit the accuracy of the lens model. Johnson & Sharon (2016) found that while the enclosed mass is well constrained at the radius of the lensing evidence, its systematic uncertainty decreases with increasing number of lensing constraints and spectroscopic redshifts. The analysis in Johnson & Sharon (2016) is tuned to the typical number of constraints in high cross-section lensing clusters such as the Frontier Fields (Lotz et al. 2016), and therefore they do not sample the effect on systematics in a case like SDSS J2222+2745, a much lower-mass cluster with four multiply imaged lensed sources and three spectroscopic redshifts. We therefore conservatively adopt a 10% systematic uncertainty on the enclosed mass, which is the typical uncertainty for a case of five sources and no spectroscopic redshifts. Interestingly, the observational measurement of the \( \tau_{AC} \) time delay places a tight constraint on the total enclosed mass and is what drives the relatively small statistical uncertainty.

Figure 5 shows the contours of the projected mass density distribution from the strong lens model and the X-ray contours from Swift observations (Section 2.3). We find that the X-ray-emitting gas and the dark matter distribution are generally aligned, with no significant offset between their centroids. A more robust measurement of the X-ray distribution will be enabled with the superior resolution of Chandra observations.

4.3. Magnification

The magnification map for a source at the quasar redshift \( z = 2.805 \), and the magnifications measured at the position of each image of the quasar are shown in Figures 7(b) and Table 4, respectively. The uncertainties are estimated by computing magnification maps for a series of lens models sampled from steps in the MCMC that correspond to 1σ in the parameter space, and the 95% confidence interval of the time delay measurements of Dahle et al. (2015). Since quasars are variable sources and are not standard candles, we cannot compare the absolute predicted magnification with an observational measurement. Nevertheless, we can compare the predictions to the relative magnifications among images A, B, and C of the quasar, for which time delays have been measured. Dahle et al. (2015) find that the light curves of images A, B, and C can be matched with time delays of \( \tau_{AB} = 47.7 \pm 6.0 \) and \( \tau_{AC} = -722 \pm 24 \), and magnitude shifts of \( \Delta \text{mag}_{AB} = 0.340 \pm 0.007 \text{ mag} \) and \( \Delta \text{mag}_{AC} = 0.483 \pm 0.012 \text{ mag} \). We find that the model is in agreement with the observed relative magnification of image A and B. The model-predicted magnification of C is \( \sim 30\% \) too high to agree with the observed magnification ratio between A and C, indicating that the systematic uncertainties may be underestimated. We note that substructure in the cluster, as well as structure along the line of sight, may contribute to discrepancy between the measured and model-derived relative magnifications.

Compared to the initial model in Dahle et al. (2013), which was based on ground-based observations, we find that the magnifications of A, B, and C are \( \sim 2.5 \times \) higher than those derived in Dahle et al. (2013), but well within the large statistical uncertainties reported there. Moreover, systematic uncertainties, which are not taken into consideration, are large for lens models that are based on few lensed sources and few spectroscopic redshifts (Johnson & Sharon 2016). We also note that the new constraints from the HST data required a more massive component at the south of the cluster (G4) to explain the lensing evidence that was not identified from the ground. Compared to the magnifications in other wide-separation lensed quasars, we find that the magnifications of A, B, and C in SDSS J2222+2745 are similar to the best-fit model-predicted magnifications of the three brightest images in SDSS JI029, from Oguri et al. (2013), while in Oguri (2010), the lens model of SDSS J1004 predicts magnifications a factor \( \sim 2 \) higher.

4.4. Source Plane Reconstruction

We reconstruct the source image of the lensed galaxy A1 at \( z = 2.3 \) and the host galaxy of the quasar at \( z = 2.805 \) by ray-tracing the image-plane pixels through the lens equation, \( \beta = \theta - \alpha(\theta) \), where \( \beta \) is the source position of each pixel, \( \theta \) is its observed position, and \( \alpha(\theta) \) is the deflection matrix scaled by \( \frac{\partial \phi}{\partial \theta} \), the ratio between the distance from the lens to the source and from the observer to the source. The high lensing magnification resolves small substructure in these galaxies, which would otherwise be too small for HST resolution. Galaxy A1 is highly distorted by the lensing potential due to its close proximity to the caustic. It is likely that a small region of this galaxy is multiply imaged within the giant arc.
Prior to ray-tracing the images, we subtract the light of the point-source quasar light and the foreground white dwarf to reveal the underlying information. In each band we select a star in the field of view with similar brightness. We generate a second image by shifting the data so that the star is at the exact pixel position of the point source we wish to mask. We then scale the shifted image and subtract it from our data. Figure 10 shows the reconstructed source-plane image of galaxy A and of the quasar host galaxy.

From the reconstructed source image, A1 measures $\sim 13$ kpc in diameter and the quasar host is measured to be $\sim 3$ kpc in diameter. A thorough investigation of the physical properties of these galaxies is left for future work.

### 4.5. Absorbing Systems

Stark et al. (2013) find strong evidence for an absorption system at $z = 2.3$ in the spectrum of image A of the quasar, indicating that an extended gas halo of a galaxy, most likely A1, has neutral hydrogen and metals, from absorption lines of Ly$\alpha$, Si $\Pi$ $\lambda 1526$, and C $\IV$ $\lambda 1549$. Stark et al. (2013) estimate the projected distance between A1 and image A of the quasar at $\sim 50$ kpc. To date, the only spectroscopically confirmed galaxy at this redshift in this field is A1; nevertheless, it is possible that another galaxy exists on this line of sight with this exact redshift.

A proper estimate of the impact parameter takes into account the path of the light from the quasar source plane to each of its images, and where these paths traverse the source plane of A1, at $z = 2.3$. In the left panel of Figure 11 we show a reconstruction of the source plane at the redshift of galaxy A1. By ray-tracing the quasar images to the same redshift of A1, we find that the quasar light passes 34 kpc north of the center of A1. At this redshift, the quasar paths are separated by as much as 5 kpc. We are therefore presented with a unique opportunity to sample the uniformity of the gas halo on scales of a few kiloparsecs, with at least three bright lines of sight.

Our GMOS multi-object spectroscopy masks targeted images A, B, C, and D of the quasar. Slits were placed on these sources on both nod and shuffle positions, and on both masks, resulting in a total of 2400 s on target for A, B, and D, and 3600 s on target for C. The wavelength coverage allows the detection of Fe $\Pi$ 2586, 2600 and Mg $\Pi$ 2796, 2803 at the redshift of A1.

The intervening absorption system is detected in the spectra of all three bright images of the quasar (A, B, C), at a redshift of $z = 2.2988 \pm 0.0002$. In the right panel of Figure 11, we plot the two strongest features of this system, the Mg $\Pi$ 2796, 2803 Å doublet and the Fe $\Pi$ 2600 Å line. The spectra were continuum normalized, with the continuum calculated by smoothing the spectra with a 40 Å boxcar.

In Table 5 we tabulate the equivalent width and redshift measurements for this absorption system in each quasar spectrum. Since the blue wing of the Mg $\Pi$ 2976 Å feature is affected by the [Ne $\IV$] and Fe $\III$ emission complex at 2423 Å rest frame (Vanden Berk et al. 2001), we do not try to fit this line, but instead consider the weaker transition Mg $\II$ 2803.

The intervening system is clearly detected in Mg $\II$ in all three images of the quasar; the weaker Fe $\II$ 2600 is detected in quasar images A and B. The equivalent widths are comparable given the uncertainties listed in Table 5. While Figure 11 shows some variation in the absorption profiles from quasar image to image, particularly in the amount of redshifted absorption, these variations may not be significant given the S/N of the data. Deeper spectra are required to measured differences in the absorption along these three lines of sight.

We also detect Fe $\II$ and Mg $\II$ absorption from a second absorber at $z = 1.202$ in the three spectra. The corresponding object is not currently identified in the imaging or spectroscopic data. The largest separation between the quasar lines of sight at this redshift is $\sim 40$ kpc.

Co-adding the spectra from the forthcoming spectroscopic follow-up campaign (Section 5) will result in a deep spectrum of each of the quasar images, and high enough S/N to determine some of the physical properties of the gas halo in the absorbing systems.

### 5. FUTURE WORK

Ongoing monitoring with the NOT (PI: Dahle) will tighten the constraints on the measured time delays. Recent observations indicate that image C of the quasar continues its brightening trend, and the measured 722 day lag provides a unique opportunity to plan future observations of A and B.
when they are at their brightest epoch. During the 2018 observing season, images A and B will both reach a level $>1.1$ magnitudes brighter than during the GMOS spectroscopic observations reported in this paper. Imaging monitoring with Gemini North (GN-2016A-Q-28; PI: Gladders) is under way to constrain the time delays between the internal three images (D, E, F) of SDSS J2222+2745. Spectroscopic monitoring with Gemini North (GN-2016B-Q-28; PI: Treu) will enable a measurement of the mass of the central black hole through reverberation mapping (Blandford & McKee 1982; Peterson 1993; Pancoast et al. 2011). In this paper, we present a revised lens model of SDSS J2222+2745 from high-resolution multiband HST imaging, new spectroscopic redshifts, and constraints from the measured time delays of three images of the background quasar. The astrophysical applications of SDSS J2222+2745 span studies of galaxy structure at small physical scales, quasar physics, and cluster astrophysics and cosmology; its investigation has just begun.

We thank the anonymous referee for useful comments, which improved this manuscript. Support for program GO-13337 was provided by NASA through a grant from the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., under NASA contract NAS 5-26555. K.E.W. gratefully acknowledges support by NASA through Hubble Fellowship grant #HF2-51368 awarded by the Space Telescope Science Institute.
Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., for NASA. Based on observations obtained at the Gemini Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc., under a cooperative agreement with the NSF on behalf of the Gemini partnership: the National Science Foundation (United States), the National Research Council (Canada), CONICYT (Chile), the Australian Research Council (Australia), Ministério da Ciência, Tecnologia e Inovação (Brazil) and Ministerio de Ciencia, Tecnología e Innovación Productiva (Argentina). This work made use of data supplied by the UK Swift Science Data Centre at the University of Leicester. This work makes use of the Matlab Astronomy Package (Ofek 2014).

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