Form-function relations in cone-tipped stimulating microelectrodes

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INTRODUCTION

Metal microelectrodes are widely used in neuroscience research, and could potentially replace macroelectrodes in various neuro-stimulation applications where their small size, specificity, and their ability to also measure unit activity are desirable. The design of stimulating microelectrodes for specific applications requires knowledge on how tip geometry affects function, but several fundamental aspects of this relationship are not yet well understood. This study uses a combined experimental and physical finite elements simulation approach to formulate three new relationships between the geometrical and electrical properties of stimulating cone-tipped tungsten microelectrodes: (1) The empirical relationship between microelectrode 1-kHz impedance and the exposed tip surface area is best approximated by an inverse square-root function (as expected for a cone-tipped resistive interface). (2) Tip angle plays a major role in determining current distribution along the tip, and as a consequence crucially affects the charge injection capacity of a microelectrode. (3) The critical current for the onset of corrosion is independent of tip surface area in sharp microelectrodes.

Keywords: microelectrodes, deep brain stimulation, cone-tipped, critical current density, finite elements model
boundary and the critical currents for the onset of microelectrode degradation. To address these issues our study combines a series of in vitro measurements using (primarily) tungsten microelectrodes, and analysis of finite elements numerical solutions for current density distributions around stimulating microelectrodes. Our study focuses on a search for generic relationships that can potentially be useful in many practical situations (using measurements from the nearly universal 1-kHz impedance testing equipment). We conclude by discussing the study’s limitations, and the relationship of our findings to the theoretical behavior of cone-shaped capacitors and resistors.

**MATERIALS AND METHODS**

**GEOMETRICAL AND ELECTRICAL MEASUREMENTS**

Forty-nine glass-insulated tungsten microelectrodes and three platinum microelectrodes (Nano-Biosensors, Nazareth, Israel) were examined. Each microelectrode was photographed using a Nikon Eclipse TS100 microscope with a Nikon Digital Sight DS-5Mc camera, and its geometry was analyzed in MATLAB R2006b (MathWorks, Natick, MA, USA). The exposed tip of the microelectrode (Figure 1A) was approximated to a simple cone whose base diameter ($D$) and distance between apex and base perimeter ($L$) were measured. The tip’s angle (the two-dimensional projection of an axisymmetric spatial angle) and surface area were calculated according to:

$$\alpha [^\circ] = \frac{360}{\pi} \arcsin \left( \frac{D}{2L} \right)$$

(1)

$$S[\mu m^2] = \frac{\pi DL}{2}$$

(2)

The combined impedance of the microelectrode and its interface with an electrolyte approximating the ionic composition of the extracellular matrix (0.15-M NaCl solution), was measured at 1 kHz using a 10-nA sine wave (FHC impedance meter).

A variable amplitude 100-Hz sinusoidal alternating current was then applied to the circuit using an analog stimulus isolator (model 2200, A-M SYSTEMS, Sequim, WA, USA), driven by a DF1643 series function generator. One-minute stimulations were repeatedly carried out with gradually increasing current amplitudes until visible damage to the microelectrode’s tip was obtained at a critical current. As the microelectrodes were delivered in different sets, the first microelectrode in each set was used to establish a rough range of damage threshold, and the rest were used to make the fine specific measurements. Twenty-two tungsten microelectrodes and three platinum microelectrodes that provided an accurate reading of damage thresholds were included in the analysis. A critical current density was calculated from the geometrical measurements as follows:

$$J_c = \frac{I_c}{S}$$

(3)

**MODELING AND SIMULATION**

Our simulations are based on an adaptation of the finite elements model of a stimulating microelectrode introduced by McIntyre and Grill (2001). Considering the frequency used for stimulation (100 Hz), the dimensions and the electrical properties of the solution (or of biological tissues) allow us to utilize a quasi-static approximation and solve the Laplace equation for the DC case (Plonsey, 1969). A cylindrical insulated microelectrode with an uninsulated cone-shaped tip was set in axial-radial coordinates (Figure 1B), and the Laplace equation:

$$\nabla \cdot \nabla V = 0$$

(4)

was solved for a surrounding conductive medium ($\sigma = 0.3$ S/m, as typical for cortex tissue – Sances and Larson, 1975) with dimensions $2 \text{ mm} \times 1 \text{ mm}$ (representing a three-dimensional cylinder of volume $2\pi \text{ mm}^3$). The microelectrode tip was set to 1 V and the edges of the surrounding medium were set to 0 V. Electrical flux perpendicular to the insulation was not allowed, and radial flux at $r = 0$ was fixed to zero due to symmetry considerations. In contrast with the model of McIntyre and Grill (2001), apex
Curvature is neglected and the surfaces of the tip and the insulation are parallel, to suit the geometry of the microelectrodes tested experimentally.

The model was solved in COMSOL Multiphysics 3.2b (COMSOL Inc., Burlington, MA, USA). The simulation resulted in a map of potentials inside the medium, from which a field of current density was derived. The current density near the tip was analyzed for different conical geometries (same angle with changing surface area, and vice versa).

RESULTS

IMPEDANCE-GEOMETRY RELATIONSHIP

The tungsten microelectrodes were classified into two major classes according to their tip angle: an acute angle class (24 microelectrodes; tip angles 41 ± 5° STD) and a nearly right-angle class (25 microelectrodes; tip angles 81 ± 5°).

To understand the dependence of microelectrode impedances on form parameters, we measured characteristic 1-kHz impedances for our entire sample. Impedances were found to be strongly related to the tip surface area ($r = 0.93$) was found between impedances and the inverse square-root of the surface area:

$$Z[\text{M} \Omega] = -0.63 + \frac{40}{\sqrt{S[\mu\text{m}^2]}}$$

(5)

Strong correlations were also found to the inverse of surface area ($r = 0.91$), in agreement with Robinson’s model (Robinson, 1968), and to the logarithm of surface area ($r = -0.92$), consistent with previous measurements (Tielen et al., 1971). Note that the predictions of inverse-root and inverse fits at 1000 $\mu$m$^2$, for instance ($Z = 627$ and $Z = 595$ k$\Omega$, respectively), are close to that of Robinson for platinum electrodes under 1-kHz stimulation – $Z = 557$ k$\Omega$ (Robinson, 1968, p. 1067). By comparing mean square errors (MSE) of the fits, the superiority of inverse-root relationship over inverse and logarithmic relationships becomes clearer (MSE = 0.114, 0.144 and 0.136, respectively). For further justification of favoring inverse-root relationship, see discussion.

We next calculated the dependence of the mean current density along the tip in the model simulation on the form parameters. Within the tip size range of 200–3000 $\mu$m$^2$, the mean current density ($J$) is nearly independent of tip angle, with relative differences between the cases of 40° and 90° of 4.8 ± 3.0%. In contrast, $J$ is strongly related to the tip surface area (Figure 2). Here too, inverse square-root relationships (Eqs 6 and 7) provide an excellent fit with the results ($r > 0.99$ for both), whereas inverse and logarithmic relationships yield weaker fits: MSE values of these fits are more than an order of magnitude larger than the MSE of the former fits (Figure 3, inset).

$$f_{\alpha} [\mu\text{A}/\mu\text{m}^2] = \frac{0.97}{\sqrt{S[\mu\text{m}^2]}} + 1.5 \times 10^{-3}$$

(6)

$$f_{\alpha} [\mu\text{A}/\mu\text{m}^2] = \frac{0.84}{\sqrt{S[\mu\text{m}^2]}} + 3.7 \times 10^{-3}$$

(7)

THRESHOLD CURRENTS FOR MICROELECTRODE DEGRADATION

Values of critical currents for microelectrode degradation were registered from experimental observations. In contrast to the impedance, the critical current and current density of the microelectrodes are considerably dependent on tip angle, as the small angle class (14 samples; tip angles 41 ± 4° STD) and the large angle class (eight samples; tip angles 83 ± 4°) exhibit an entirely different behavior from each other. We find that the critical current density has a clear

![Figure 2](image1.png)  
**FIGURE 2** Impedance of electrode-electrolyte complex vs. tip surface area of tungsten microelectrodes, with possible inverse and inverse-root relationships. Inset: Logarithmic relationship, in logarithmic scale.

![Figure 3](image2.png)  
**FIGURE 3** Mean current density vs. tip surface area, as predicted by simulation for two extreme cases of tip angle – 40° and 90°. Inset: MSE of three different fits: (1) inverse root, (2) inverse and (3) logarithmic.
Tungsten

Large tip angle
drops along with increase in impedance (relationship: refer to as outliers):

\[ J_{\text{cr},W} [\mu \text{A/\mu m}^2] = \frac{4.5}{S[\mu \text{m}^2]} \]  

An inverse relation to increasing surface area was also obtained for the three platinum microelectrodes tested under the same conditions \((r > 0.99, \text{tip angles: } 82, 84 \text{ and } 90):\)

\[ J_{\text{cr},Pt} [\mu \text{A/\mu m}^2] = \frac{8.5}{S[\mu \text{m}^2]} \]  

Critical current density of small angle tungsten specimens showed no significant dependence on either surface area or impedance.

As for critical current, in the small angle class it substantially drops along with increase in impedance (Figure 4B) and an inverse relationship:

\[ I_{\text{cr,small}} [\mu \text{A}] = \frac{0.77}{Z[M\Omega]} \]  

was found to best fit the results \((r = 0.94)\), whereas in the large angle class the critical current showed no significant relation to impedance, nor to surface area. Specifically, all specimens resisted corrosion until current reached 4–5 \(\mu\)A except for the two above-mentioned outliers which underwent corrosion at 1–1.5 \(\mu\)A (despite the fact that they were not exceptional in terms of neither impedance nor surface area), suggesting that these microelectrodes may have been defective.

**EFFECT OF CRITICAL REGIONS**

To gain a better understanding of the tip behavior under the application of current, we analyzed the spatial distribution of current densities near the tip in our numerical solutions. Simulation results (Figures 5A,B) show that the computed current distributions along the tip is far from being uniform and is characterized by two regions of high current density: the apex of the cone (hereinafter: tip head) and the perimeter of its base where the metal becomes exposed (hereinafter: end of insulation). This observation coincides with the numerical results obtained by Gimsa et al. (2006). Since corrosion is expected to commence where current density is the highest, these regions will be referred to as “critical regions”.

Indeed, during stimulation we experimentally observed the formation of bubbles at these regions (Figure 5C). Gaseous bubbles (of hydrogen, oxygen or chlorine) are formed as a result of the solution’s hydrolysis and occur first at the regions where current density is highest.

The critical regions were under scrutiny when numerically analyzing changes in current density with respect to the tip’s cone parameters. The current density at these regions was computed for a spectrum of angles so as to explore the source for differences in behavior between acute angle tips and right-angle tips. In order to isolate the effect of tip angle, surface area was held constant and shows that the current density at the tip head substantially increased, whereas for the smaller angle current density at end of insulation remains higher than that at tip head for all angles, whereas for the smaller surface area the inequality reverses for small angles. A transition range exists between 40° and 50°, with 46° being the intersection of the two corresponding linear fits. Such observation can certainly account for the different behavior exhibited by the two classes of microelectrodes, since the two classes are on opposite sides of the “turnover” angle: \((41 \pm 4°) \leq 46 \leq (83 \pm 4°)\).

A graphical visualization of the entire current density distribution along tips of two representative types (90° and 40°) is shown in Figures 5A,B, and shows that the current density at the tip head is substantially reduced as a result of tip blunting.

In order to isolate the effect of surface area, current density was examined at the two critical zones for two different cases of constant tip angle – 90° (Figure 7A) and 40° (Figure 7B). The simplest relationships that fitted all four simulations sufficiently well \((|r| \geq 0.95)\) were inverse-root:

**FIGURE 4 | (A) Critical current density of large tip angle species vs. tip surface area, with inverse fits (putative outliers are excluded). (B) Critical current for corrosion of tungsten microelectrodes vs. impedance of electrode-electrolyte complex, with possible inverse relationship for species with small tip angle.**
approach. Our experimental sample consisted of tungsten microelectrodes with sharp or right-angled tips, and with surface areas that varied over 1.5 orders of magnitude (100–2700 μm²). Our results provide new insights regarding these dependences that may also assist the design of microelectrodes for safe and efficacious stimulation of neural tissue.

We first compared three different functional relationships for the experimentally derived dependence between the impedance Z(1 kHz) and tip surface area S: a logarithmic relationship (obtained by Tielen et al., 1971), an inverse relationship (implied by the model of Robinson, 1968), and an inverse-root relationship. To the best of our knowledge, such comparison was not made before the present work. The inverse square-root relationship

\[ j_{90^\circ, \text{apex}} \cdot j_{90^\circ, \text{base}} \cdot j_{40^\circ, \text{apex}} \cdot j_{40^\circ, \text{base}} \propto \frac{1}{\sqrt{S}} \]  

(with different proportionality constants) and logarithmic, although the latter cannot apply for large values of surface area (otherwise implying negative current densities) and thus their validity is restricted.

DISCUSSION

MAIN CONTRIBUTIONS

In this study, we systematically examined the dependence of certain electrical properties of metal microelectrodes on the geometry of the exposed tip, using a combined experimental and simulation approach.
The conical microelectrode geometry studied here renders the full theoretical analysis of the problem quite complicated. Nevertheless, certain approximate solutions can provide additional insights into the validity of our experimental and simulation results. The electrochemical double-layer can be seen as a capacitor with conical equipotentials, an inverse-root relationship with respect to the surface area can be derived:

$$R = \frac{\cos(\theta/2)^{2}}{\sigma \pi h} \approx \frac{\cos(\theta/2) \sqrt{\sin(\theta/2)}}{\sigma \sqrt{\pi S}} \approx \frac{1}{S}$$

(Eq. 5) yielded the best fit (Figure 2). This functional form is also consistent with our model simulation results, where the mean current density \(I\) was found to vary as \(1/\sqrt{S}\) irrespective of tip angle (Figure 3), thus predicting the same relation for the impedance itself:

$$Z(V, I) = \frac{V}{I} = \frac{V}{J \cdot S} \approx \frac{1}{\sqrt{S}}$$

(where \(V\) is a constant voltage). The fact that inverse-root fit was significantly better than other fits for simulated mean current density (Figure 3) strengthens the certainty about inverse-root relationship for measured impedance (Figure 2).

The conical microelectrode geometry studied here renders the full theoretical analysis of the problem quite complicated. Nevertheless, certain approximate solutions can provide additional insights into the validity of our experimental and simulation results. The electrochemical double-layer can be seen as a capacitor with two cone-shaped plates. The analytical solution for a minimally-trimmed cone capacitor was derived by Selby (1962):

$$C = \frac{2\pi \varepsilon h}{\ln \left[1 + 2(D/h)\cos(\theta/2)\right]} = \frac{\pi \varepsilon h^{2}}{D \cos(\theta/2)^{2}}$$

where \(\varepsilon\) is the medium’s absolute permittivity, \(h\) is the trimmed cone’s height, \(D\) is the distance between the imaginary apices of the cones and \(\theta\) is the cones angle. Since the surface area of a minimally-trimmed cone practically equals \(\pi h^{2} \tan(\theta/2)/\cos(\theta/2)\), the following relation is derived for the impedance:

$$|Z| = \frac{1}{\omega C} = \frac{D \sin(\theta/2)}{\omega \varepsilon \cdot S} \approx \frac{1}{S}$$

This solution does not take into consideration the shunt capacitance introduced in models of the interface (e.g., Robinson, 1968).

In contrary, analysis of resistance relates solely to the surrounding medium, as interfacial currents are strictly capacitive under the low currents used in impedance measurements. When neglecting fringe effects and assuming current spread in an infinite medium with conical equipotentials, an inverse-root relationship with respect to the surface area can be derived:

$$R = \frac{\cos(\theta/2)^{2}}{\sigma \pi h} \approx \frac{\cos(\theta/2) \sqrt{\sin(\theta/2)}}{\sigma \sqrt{\pi S}} \approx \frac{1}{S}$$

This analytical result is in agreement with the inverse square-root relationship found in the simulation results where a resistive medium was assumed. In the experimental measurements, both the resistive medium and the capacitive interface play a role in determining the impedance. The better experimental fit of the inverse-root functional may imply that the effect of the medium on the impedance is stronger than that of the interface.

A second major focus of our study was on thresholds for microelectrode degradation, for which the direct implication is corrosion of the metal. Degradation might also be accompanied by other Faradaic processes and the formation of free radicals which are hazardous for the living tissue. Both experimental and simulation results demonstrated a significant disparity between the properties of sharper tips (~40°) and blunter tips (~90°). The constant critical current for blunt tips is surprising, implying that larger tip would not improve the microelectrode’s endurance. The calculation of critical current density (Eq. 3) refers only to mean density, whereas corrosion selectively begins at critical regions where current density is much higher. Most of the current flows through a small fraction of the surface, hence an increase in surface area contributes mostly to regions of low current density. As a result, enlarging the surface only moderately affects current densities at critical regions while significantly decreasing critical mean current density. This coincides with the different relationships obtained both experimentally (Figure 4A) and in simulation (Figure 7): current densities at critical regions moderately
decline with increase in surface area (varying as $1/\sqrt{S}$), whereas critical mean current density drops more rapidly (varying as $1/S$). Our results thus support and extend McIntyre and Grill’s (2001) observation that peak current density is not linearly proportional to the change in surface area.

**METHODOLOGICAL CHOICES AND THEIR GENERALITY**

We have attempted to study generic, practical aspects of form-function relations in stimulating microelectrodes. This has led us to focus on 1-kHz impedances, universally used to qualitatively characterize microelectrodes in both laboratory and clinical settings. Clearly, a more thorough impedance spectroscopy treatment is needed in order to understand how our observations are related to the (generally frequency-dependent, non-linear and non-stationary) microelectrode properties (e.g., Gimsa et al., 2005). Moreover, the proposed relationships describing 1-kHz impedance are relevant in a wide range of measured surface area (100–2700 μm²) but are not necessarily valid outside this range. Indeed, some of the functional forms we have obtained imply physically impossible negative impedances for very large tips.

The study of microelectrode degradation focused on the properties of tungsten microelectrodes using 100-Hz sinusoidal stimulation. Pulse frequencies of approximately 100 Hz (typical range: 90–130 Hz) are most commonly used in DBS stimulation paradigms, and driving the electrodes with sinusoidal currents (rather than low duty-cycle pulses used for neuro-stimulation) simply accelerates the electrodes’ degradation. Tungsten microelectrodes are typically only used for stimulation in undemanding acute studies due to their relatively low damage thresholds. We therefore also measured a small sample of platinum microelectrodes, and contrasted the empirical results with the behavior of physical models, overall suggesting that our results appear to be material-independent. Nevertheless, it will be interesting to test whether the more clinically useful platinum/iridium microelectrodes manifest similar degradation modes and characteristics.

**ACKNOWLEDGMENTS**

We thank Mr. Nabil Jadaon and Dr. Emad Nimer of Nano Biosensors Ltd. for many helpful discussions and for providing the electrodes, and Dr. Oscar Lichtenstein for making available some of the equipment. We would like to acknowledge Dr. Victor Pikov and the reviewers for their important comments on the manuscript, and the support provided by Israeli Science Foundation grant #1248/06 and European Research Council starting grant #211055.

**SUPPLEMENTARY MATERIAL**

The Supplementary Material for this article can be found online at http://www.frontiersin.org/neuroengineering/paper/10.3389/neuro.16/013.2009/

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**Conflict of Interest Statement:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as potential conflict of interest.