Galaxy growth in a massive halo in the first billion years of cosmic history

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According to the current understanding of cosmic structure formation, the precursors of the most massive structures in the Universe began to form shortly after the Big Bang, in regions corresponding to the largest fluctuations in the cosmic density field1–3. Observing these structures during their period of active growth and assembly—the first few hundred million years of the Universe—is challenging because it requires surveys that are sensitive enough to detect the distant galaxies that act as signposts for these structures and wide enough to capture the rarest objects. As a result, very few such objects have been detected so far4,5. Here we report observations of a far-infrared-luminous object at redshift 6.900 (less than 800 million years after the Big Bang) that was discovered in a wide-field survey6. High-resolution imaging shows it to be a pair of extremely massive star-forming galaxies. The larger is forming stars at a rate of 2,900 solar masses per year, contains 270 billion solar masses of gas and 2.5 billion solar masses of dust, and is more massive than any other known object at a redshift of more than 6. Its rapid star formation is probably triggered by its companion galaxy at a projected separation of 8 kiloparsecs. This merging companion hosts 35 billion solar masses of stars and has a star-formation rate of 540 solar masses per year, but has an order of magnitude less gas and dust than its neighbour and physical conditions akin to those observed in lower-metallicity galaxies in the nearby Universe7. These objects suggest the presence of a dark-matter halo with a mass of more than 100 billion solar masses, making it among the rarest dark-matter haloes that should exist in the Universe at this epoch.

SPT0311–58 (SPT-S J031132–5823.4) was originally identified in the 2,500-deg² South Pole Telescope (SPT) survey6,9 as a luminous source (flux densities of 7.5 mJy and 19.0 mJy at wavelengths of 2.0 mm and 1.4 mm, respectively) with a steeply increasing spectrum, indicative of thermal dust emission. Observations with the Atacama Large Millimeter/submillimeter Array (ALMA) provide the redshift of the source. The J = 6–5 and J = 7–6 rotational transitions of the carbon monoxide molecule and the P1–P1 fine-structure transition of atomic carbon were found redshifted to 87–103 GHz in a wide spectral scan8.

The frequencies and spacings of these lines unambiguously place the galaxy at a redshift of z = 6.900(2), which corresponds to a cosmic age of 780 Myr (using cosmological parameters10 of Hubble constant $H_0 = 67.7 \pm 2.4$ km s⁻¹ Mpc⁻¹, matter density $\Omega_m = 0.309$ and vacuum energy density $\Omega_{\Lambda} = 0.691$). An elongated faint object is seen at optical and near-infrared wavelengths, consistent with a nearby edge-on spiral galaxy at z = 1.4 ± 0.4 that acts as a gravitational lens for the background source (see Methods section ‘Modelling the SED’; here and elsewhere the error range quoted corresponds to a 1σ uncertainty). Together, these observations indicate that SPT0311–58 is the most distant known member of the population of massive, infrared-bright but optically dim, dusty galaxies that were identified from ground- and space-based wide-field surveys11.

The far-infrared emission from SPT0311–58 provides an opportunity to study its structure with little confusion from the foreground galaxy. We conducted ALMA observations at about 0.3º resolution at three different frequencies (see Methods): 240 GHz, 350 GHz and 420 GHz, corresponding to rest-frame wavelengths of 160 μm, 110 μm and 90 μm. The observations at 240 GHz include the 18μm fine-structure line of ionized carbon ([C ii]) and those at 420 GHz the 88μm fine-structure line of doubly ionized oxygen ([O iii]). The 160μm continuum and the [C ii] and [O iii] fine-structure line emission maps of the source are shown in Fig. 1. Two emissive structures are visible in the map, denoted SPT0311–58 E and SPT0311–58 W, which are separated by less than 2º on the sky before correction for gravitational deflection. Although the morphology of SPT0311–58 E and SPT0311–58 W is reminiscent of a lensing arc (SPT0311–58 W) and counter-image (SPT0311–58 E), the [C ii] line clarifies the physical situation: SPT0311–58 E is separated from the brighter source SPT0311–58 W by 700 km s⁻¹ and is therefore a distinct galaxy.

Lens modelling of the 160-μm, 110-μm and 90-μm continuum emission from SPT0311–58 was performed using a pixelated reconstruction technique12 (Fig. 1c, Extended Data Fig. 5, Methods section ‘Gravitational lens modelling’). Its structure and lensing geometry is consistent between the observations, and indicates that the two galaxies are separated by a projected (proper) distance of 8 kpc in the

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source plane. SPT0311−58 E has an effective radius of 1.1 kpc, whereas SPT0311−58 W has a clumpy, elongated structure that is 7.5 kpc across.

The (flux-weighted) source-averaged magnifications of each galaxy and of the system as a whole are quite low ($\mu_E = 1.3, \mu_W = 2.2, \mu_{tot} = 2.0$) because SPT0311−58 W is extended relative to the lensing caustic and SPT0311−58 E is far from the region of high magnification. The same lensing model applied to the channelized [C ii] data reveals a clear velocity gradient across SPT0311−58 W, which could be due to either rotational motions or a more complicated source structure coalescing at the end of a merger.

Having characterized the lensing geometry, it is clear that the two galaxies that comprise SPT0311−58 are extremely luminous. Their intrinsic infrared (8−1000 $\mu$m) luminosities have been determined from observations of rest-frame ultraviolet-to-submillimetre emission (see Methods section ‘Modelling the SED’) to be $L_{IR} = 4.6(\pm 1.2) \times 10^{12} L_{\odot}$ and $L_{IR} = (33 \pm 7) \times 10^{11} L_{\odot}$ for SPT0311−58 E and SPT0311−58 W, respectively, where $L_{\odot}$ is the luminosity of the Sun. Assuming that these sources are powered by star formation, as suggested by their extended far-infrared emission, these luminosities are unprecedented at $z > 6$. The implied (magnification-corrected) star-formation rates are correspondingly enormous—$(540 \pm 175) M_{\odot} \text{yr}^{-1}$ and $(2,900 \pm 1,800) M_{\odot} \text{yr}^{-1}$, where $M_{\odot}$ is the mass of the Sun—probably owing to the increased instability associated with the tidal forces experienced by merging galaxies. The components of SPT0311−58 have luminosities and star-formation rates similar to the other massive, $z > 6$ galaxies identified by their dust emission, including HIFL3 (z = 6.34), which has a star-formation rate of $1,300 M_{\odot} \text{yr}^{-1}$ after correcting for a magnification factor of 2.2, and a close quasar-galaxy pair at $z = 6.59$, the components of which are forming stars at rates of $1,900 M_{\odot} \text{yr}^{-1}$ and $800 M_{\odot} \text{yr}^{-1}$, respectively. However, unlike the latter case, there is no evidence of a black hole in either source in SPT0311−58.

Unlike any other massive dusty source at $z > 6$, the rest-frame ultraviolet emission of SPT0311−58 E is clearly detectable with modest integration by the Hubble Space Telescope. The detected ultraviolet luminosity ($L_{UV} = (7.4 \pm 0.7) \times 10^{10} L_{\odot}$) suggests a star-formation rate of only $13 M_{\odot} \text{yr}^{-1}$, 2% of the rate derived from the far-infrared emission, consistent with SPT0311−58 E forming most of its stars behind an obscuring veil of dust. The inferred stellar mass for this galaxy (see Methods section ‘Modelling the SED’) is $(3.5 \pm 1.5) \times 10^{10} M_{\odot}$. Although no stellar light is convincingly seen from SPT0311−58 W, the absence of rest-frame ultraviolet emission is probably explained by heavy dust
obscuration and is not unusual. Although SPT0311–58 E is the least massive of the two components, even it is rare among ultraviolet-detected galaxies at \( z \approx 7 \). Such galaxies are found in blank-field surveys to have a sky density of just one per 30 square arcminutes.

The far-infrared continuum and line emission of SPT0311–58 E and SPT0311–58 W (Fig. 1d–f) imply substantial differences in the physical conditions in these objects. Compared to SPT0311–58 W, SPT0311–58 E has a higher ratio of \([\text{C} \, \text{II}]\) line emission to 160-\( \mu \)m continuum emission and a much larger luminosity ratio between \([\text{O} \, \text{III}]\) and \([\text{C} \, \text{II}]\). The \([\text{O} \, \text{III}]\) emission is much more luminous in SPT0311–58 E, with most of SPT0311–58 W (excluding the southern end) showing no emission at all. Because the formation of \( \text{O}^++\) ions requires photons with energies of more than 35.1 eV, this line arises only in ionized regions around the hottest stars and near active galactic nuclei. It is unlikely that active galactic nuclei are the origin of the \([\text{O} \, \text{III}]\) line in SPT0311–58 E, because the continuum and line emission both extend across most of the galaxy rather than being concentrated in a putative nuclear region. Observations of \([\text{O} \, \text{III}]\) 88-\( \mu \)m emission in actively star-forming galaxies at low- and high-redshift have found that the line luminosity ratio between \([\text{O} \, \text{III}]\) and \([\text{C} \, \text{II}]\) increases as gas metallicity decreases. The ultraviolet photons capable of forming \( \text{O}^++\) have a longer mean free path in a lower-metallicity interstellar medium than in a higher-metallicity one, and the electron temperature remains higher for the same ionizing flux, both of which favour increased \([\text{O} \, \text{III}]\) emission. The difference in the \([\text{C} \, \text{II}]\) line-to-continuum ratio may result from multiple effects: the known suppression of the \([\text{C} \, \text{II}]\)-to-\( L_{\text{IR}} \) ratio in regions of increased star-formation surface density (higher in SPT0311–58 E) and the increased \([\text{C} \, \text{II}]\)-to-\( L_{\text{IR}} \) ratio in star-forming galaxies of lower metallicity. Whether SPT0311–58 E (or the southern end of SPT0311–58 W, which is similar to SPT0311–58 E in these properties) has a more primordial interstellar medium than does the bulk of SPT0311–58 E can be tested with future observations.

The masses of the components of SPT0311–58 are remarkable for a time only 780 Myr after the Big Bang. In Fig. 2 we compare SPT0311–58 to objects at \( z > 5 \) for which we have estimates of dust mass \( (M_{\text{dust}}) \) or total gas mass \( (M_{\text{gas}}) \). For SPT0311–58, the best constraints on both of these quantities come from the joint analysis of its far-infrared continuum and line emission, specifically the rotational transitions of carbon monoxide and neutral carbon. Here we have divided these masses between the two galaxies according to the lensing-corrected ratio of dust continuum emission (6.7) that we determined from our three high-resolution ALMA continuum observations because the dust continuum luminosity is roughly proportional to the dust mass. The corresponding dust and gas masses for SPT0311–58 E are \( M_{\text{dust}} = (2.7 \pm 1.7) \times 10^{11} M_{\odot} \) and \( M_{\text{gas}} = (2.5 \pm 1.6) \times 10^{11} M_{\odot} \), and for SPT0311–58 W they are \( M_{\text{dust}} = (0.4 \pm 0.2) \times 10^{11} M_{\odot} \) and \( M_{\text{gas}} = (0.4 \pm 0.2) \times 10^{11} M_{\odot} \). The gas mass can also be estimated using the carbon monoxide luminosity, although the conversion between luminosity and gas mass in this optically thick line is known to vary substantially depending on many factors, including star-formation intensity and metallicity. Taking the observed luminosity in the \( J = 3–2 \) line of carbon monoxide, converting it to \( J = 1–0 \) under the conservative assumption of thermalized emission, and connecting luminosity to mass using a standard value of \( \alpha_{\text{CO}} = 1.0 M_{\odot} (K \, \text{km s}^{-1} \text{pc}^2)^{-1} \), we derive \( M_{\text{gas}} = (6.6 \pm 1.7) \times 10^{10} M_{\odot} \) for SPT0311–58 W and \( M_{\text{gas}} = (1.0 \pm 0.3) \times 10^{10} M_{\odot} \) for SPT0311–58 E. The gas mass of SPT0311–58 W is well above those of all of the known galaxies at \( z > 6 \), that is, during the first approximately 900 Myr of cosmic history.

SPT0311–58 highlights an early and extreme peak in the cosmic density field and presents an opportunity to test the predictions for the growth of structure in the current cosmological model. The mass of the dark-matter halo that hosts SPT0311–58 is uncertain, but can be estimated in several ways. For most massive star-forming galaxies, the gas mass represents the dominant component of baryons that have cooled and assembled at the centre of the dark-matter halo. In this case, for the lower \( \alpha_{\text{CO}} \)-based estimate of gas mass, the cosmic baryon fraction \( f_{\text{b}} = 0.19 \) places a hard lower bound on the total halo mass of \( 4 \times 10^{11} M_{\odot} \). A less conservative assumption incorporates the knowledge, based on observations across a wide range of redshifts, that only a fraction of the baryons in a dark-matter halo (less than one-quarter, \( M_{\text{h}} / M_{\text{h}} = 0.05 \), see figure 15 of ref. 3) are destined to accrete to the stellar mass of the central galaxy. In this case, a total halo mass of \( (1.4–7.0) \times 10^{12} M_{\odot} \) is implied, depending on which estimate of gas mass is adopted. To understand the rareness of the dark-matter halo that hosts SPT0311–58, we calculate curves that describe the rarest haloes that should exist in the Universe at any redshift. In Fig. 3, we show the halo masses that are inferred for many high-redshift galaxies, using the same methods for converting gas mass to halo mass as described above. We find that SPT0311–58 is indeed closest to the exclusion curves and therefore marks an exceptional peak in the cosmic density field at this time in cosmic history.

We have found a system of massive, rapidly star-forming, dusty galaxies at \( z = 6.900 \), the most distant galaxies of this type discovered so far. Two compact and infrared-luminous galaxies are seen, separated by less than 8 kpc in projection and 700 km s\(^{-1}\) in velocity, probably in the process of forming one of the most massive galaxies of the era. Even before coalescence, the larger galaxy in the pair is more massive than any other known galaxy at \( z > 6 \). Although the discovery of such
Figure 3 Halo masses for rare, high-redshift, massive galaxies. The mass of the dark-matter halo ($M_{\text{halo}}$) defined at a density of 200 times the mean density of matter in the Universe) is inferred for galaxies in the first 2 Gyr after the Big Bang (see Methods). These masses present a range of lower limits, from the most conservative assumption (lower bars) that all baryons in the initial halo have been accounted for in the molecular gas mass to the observationally motivated assumption (upper bars) that all baryons in the initial halo have been accounted for in the cold dark matter halo ($\Lambda$). Halo masses for rare, high-redshift, massive galaxies.

Online Content Methods, along with any additional Extended Data display items and Source Data, are available in the online version of the paper; references unique to these sections appear only in the online paper.

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Author Contributions D.P.M. proposed the ALMA [C II] and [O III] line observations and analysed all ALMA data. J.S.S. performed the lens modelling. C.C.H. led the rareness analysis. M.L.N.A., M.B.B., S.C.C., A.H.G., J.M.R. and B.S. provided optical and infrared data reduction and de-convolution. K.A.P. and J.D.V. performed SDM modelling of the sources and lens. A.W. performed joint dust and high-redshift targets. D.P.M. wrote the manuscript. J.S.S., C.C.H., D.P.M., S.L.K., K.C.L. and J.D.V. prepared the figures. All authors discussed the results and provided comments on the paper. Authors are ordered alphabetically after J.D.V.

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METHODS

ALMA millimetre and submillimetre interferometry. We acquired four observations of SPT0311—58 with ALMA in four receiver bands (B3, B6, B7 and B8, covering 84–432 GHz) under projects 2015.1.00504.S and 2016.1.01293.S. A summary of these observations, including dates, calibration sources, integration times, atmospheric opacity, noise levels and resolution, is provided in Extended Data Table 1. Salient details are provided below for each observation.

The redshift of SPT0311—58 and the 3-mm continuum flux density were determined from an 84.2–114.9-GHz spectrum assembled from five separate tunings in ALMA band 3 under ALMA Cycle 3 project 2015.1.00504.S. The observing strategy has been used to discover the redshifts of more than 50 SPT dusty sources, and further details on the redshift coverage are provided in previous works.10,31 Data were taken on 2015 December 28 and 2016 January 2 in ALMA configuration C36-1 (baseline lengths of 15–310 m) using 34 and 41 antennas, respectively. The resulting image has a resolution of 3.3″ × 3.5″, although there is spatial information on finer scales that allows us to extract flux densities separately for the E and W sources, which are separated by about 2″. Further details of the analysis are provided elsewhere.32

ALMA observed SPT0311—58 a second time under project 2015.1.00504.S in band 7 (LO = 343.48 GHz) to produce a continuum image suitable for gravitational lens modelling. Similar observations were used to produce lens models of SPT sources in previous cycles.24,32 The observations were performed with 41 antennas in the C40-4 configuration, providing 15–770-m baselines. The resulting image has an angular resolution of 0.3″ × 0.5″, although, because it lacks any spectral lines, it was found to be insufficient to provide an unambiguous determination of the lensing configuration.

The ALMA Cycle 4 project 2016.1.01293.S was intended to follow up on the discovery of this very distant source through spectroscopic observations. The 158-μm continuum of SPT0311—58 was observed on 2016 November 3 in ALMA configuration C40-5, which provided baseline lengths of 18–1,120 m. This provides the primary imaging for this work, because it yielded an extremely sensitive detection of the [C II] line and continuum structure at high resolution.

A final observation was obtained in ALMA band 8 (LO = 423.63 GHz), in configuration C40-4 (baselines 15–920 m). The observations were repeated in four segments to yield the required integration time. The resulting data have 0.2″ × 0.3″ resolution. These data provide a final spatially resolved continuum observation, at 90-μm rest-frame wavelength, along with spectroscopic images of the 88-μm line of [O I] in the ALMA continuum images are shown in Extended Data Fig. 1. Star formation at 10° east of north and the instrument configured with the R400 grating and 2 × 2 detector binning. For a source that fills the 1″ slit this set-up results in a spectral resolution of about 7 Å. The observations were spatially dithered, using two central wavelength settings (8,300 Å and 8,400 Å) to cover the chip gaps. The data comprise a series of individual 900-s exposures, dithering the source spatially between two positions (X and Y) along the slit in an ABBA pattern, repeated four times, two at each central wavelength setting. The total integration time is 4 h.

The broad foreground source was positioned along the slit midway between the acquisition star and SPT0311—58, providing an additional reference point for locating traces along the slit. The spectra were reduced, beginning with bias subtraction and bad pixel masking using the IRAF GMOS package provided by Gemini. The individual chips were combined into a single mosaic for each exposure and the masqueraded frames were then sky-subtracted by differencing neighbouring A–B exposure pairs; this method resulted in nearly Poisson noise, even under the numerous bright sky lines. A flat-field slit illumination correction was applied and a wavelength calibration derived for each mosaic. The two-dimensional spectrum was created by median-combining the individual exposure frames.

The spectrum shows a faint continuum beginning above 9,000 Å at the location of SPT0311—58. A one-dimensional extraction of the faint trace yields no reliable redshift measurement, but is consistent with the redshifted 4,000–Å break that is expected for the foreground galaxy at z = 1.4. Calibrated against the nearby R = 16.4 star spectrum we find no flux at the expected location of Lyα redshifted to z = 6.900 (about 9,600 Å) down to a 3σ flux limit of 3.0 × 10^{-17} erg s^{-1} cm^{-2} for a emission line 500 km s^{-1} wide.

Image de-blending. At the position of SPT0311—58, our optical and infrared images (Extended Data Fig. 2) show a prominent lower-redshift galaxy that is responsible for lensing the source, and the HST images, which have the highest resolution, show direct stellar emission from the E source (Extended Data Fig. 3). To extract reliable photometry for SPT0311—58 E, particularly in the low-resolution Spitzer images that cover the rest-frame optical, and to search for emission from the W source underneath the lens galaxy, we must model and remove the lens emission. We follow procedures similar to those used previously,41 using the HST/WFC3 images as the source of the lens galaxy model to de-blend the IRAC image. The foreground lens can be fitted with a single Sérsic profile with an index $n = 1.77$. As seen in Extended Data Fig. 4, there is no clear rest-frame ultraviolet emission from SPT0311—58 W in the HST bands after removal of the lens source. To account for the lens from the IRAC image, the WFC3 model is convolved with the IRAC point spread function and then subtracted from the 3.6-μm and 4.5-μm images. Residual emission is seen near the positions of the E and W sources. Unfortunately, because SPT0311—58 W lies right on top of the lens, the residuals are extremely susceptible to image de-convolution errors and we do not believe

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In addition to the ALMA data, we use Herschel photometry to constrain the SED of SPT0311–58 E and SPT0311–58 W to rest-frame 30 μm (250 μm observed). The resolution of Herschel SPIRE is not adequate to separate the two components, so we divide the total flux density observed in the three SPIRE bands between the E and W sources according to the ratios observed in the ALMA bands. These photometric points are then corrected for the continuum magnification derived from the ALMA data and used in the SED modelling described below. The total and intrinsic flux densities are reported in Extended Data Table 3.

Modeling the SED. In Extended Data Fig. 7 we present the SEDs of SPT0311–58 E, SPT0311–58 W and the foreground lens galaxy.

A photometric redshift for the lens is calculated with EAZY using the data in Extended Data Table 2. The resulting redshift is 1.43, with a 1σ confidence interval of 1.08–1.85. The lens SED fitting is performed with the Code Investigating GALaxy Emission (CIGALE45,46) assuming $z = 1.43$.

The multiple rest-frame ultraviolet to rest-frame optical detections of SPT0311–58 E allow us to constrain the stellar mass using reasonable assumptions about the star-formation history at this early point in cosmic history. The SED is fitted by varying the e-folding time and age of a previously reported stellar population model47 under single- and two-component formation histories, assuming solar metallicity and previously reported42 initial mass function. The minimum radiation field, power-law slope and gamma, the fraction of dust mass exposed to radiation intensities above the minimum, from one dust model48, and the colour excess and attenuation slope from other dust models49,50 are kept free in the SED fitting. The AGN contribution is set to zero because there are no photometric points to constrain the spectral range that is most affected by AGN power (mid-infrared) and thus any fraction between 0% and 60% of the dust luminosity is attributable to AGNs with nearly equal probability. However, this ignores the spatial distributions of the dust and line emission, which are not strongly peaked as is usually observed in AGN-dominated galaxies, so we deem this wide range to be unphysical. The inferred stellar mass and star formation rates are $(3.5 \pm 1.5) \times 10^{10} M_\odot$ and $(540 \pm 175) M_\odot \, \text{yr}^{-1}$, respectively, for the two-component star-formation history. These values agree within the uncertainties for a single-component star-formation history. The infrared luminosity ($L_{\text{IR}}$, integrated over $8–1000 \mu m$) is $(4.6 \pm 1.2) 	imes 10^{12} L_\odot$ and the extinction is $A_V = 2.7 \pm 0.2$ mag.

For the W source, we have only upper limits and the potentially contaminated IRAC detections to constrain the rest-frame optical and ultraviolet emission. Accordingly, we use the IRAC photometry as upper limits, along with the HST limits and far-infrared data in Extended Data Table 3, and model the SED with CIGALE. We find a luminosity of $L_{\text{IR}} = (33 \pm 7) \times 10^{12} L_\odot$ seven times larger than for the E source. A consistent luminosity is obtained by fitting the far-infrared SED with a modified blackbody51. The inferred star-formation rate, which is closely connected to $L_{\text{IR}}$, is $(2,900 \pm 1,800) M_\odot \, \text{yr}^{-1}$. As for the E source, the AGN fraction to fall between 0% and 60% with roughly equal probability, so we take the absence of a dominant infrared emission region (see Fig. 1c and Extended Data Fig. 5) as an indication that the AGN contribution is unlikely to be important and fix the AGN fraction to zero.

The dust luminosity due to star formation could therefore be up to a factor of two smaller if the spatial distribution of the emission is ignored. Given that the photometry reaches to only the rest-frame V band, it is possible to hide a very large stellar mass behind dust obscuration for plausible values of the visual extinction ($A_V \leq 6$, as seen in other massive dusty galaxies44,46,52,53). Considering the IRAC flux densities alone, we can calculate rest-frame mass-to-light ratios for the observed bands to see what masses could exist without relying on the poorly constrained CIGALE SED modelling. We use a stellar population synthesis code54,55 to compute a stellar mass-to-light ratio under a range of assumptions: stellar ages of 0.1–6.8 Gyr (from a reasonably ‘young’ population to the approximate age of the Universe at the time), mean metallicities (attained through the luminous dust emissions), and the time in the mass range $2 \times 10^8 M_\odot$ per $L_\odot$ of measured flux density. Taking the measured and de-minified flux density (averaged between the two wavelengths) of 0.5 $\mu m$, we find a stellar mass of $(1–5) \times 10^{10} M_\odot$ before correcting for extinction. If the extinction is as large as 5 mag, the true stellar mass could be unphysically large ($>10^{12} M_\odot$), demonstrating that we have no useful constraint without greater certainty about the reliability of the IRAC flux densities or more photometric data points.

Galaxy and halo masses. In Figs 2 and 3 we compile mass measurements for high-redshift galaxies discovered through various techniques. The galaxy sample comprises primarily the galaxies identified through their luminous dust emission (DSFGs) and optically identified quasars (QSOs), which are typically the objects with the largest gas, dust or stellar masses at these redshifts. At the very highest redshifts, where very few galaxies have been found, objects selected on the basis of their ultraviolet emission are also included. The subsets of galaxies included in each

the Spitzer/IRAC fluxes to be reliable. By contrast, SPT0311–58 E is one full IRAC resolution element, 1.7″, from the lens centroid, and we consider the residual emission at this position to be usable in our subsequent analyses. Images of the model and residuals are provided in Extended Data Fig. 4 and the resulting photometry is provided in Extended Data Table 2.

Gravitational lens modelling. Gravitational lens modelling of SPT0311–58 was performed using two different codes which model the source-plane emission in different ways. Both codes fit to the visibilities measured by ALMA or other interferometers, but they do not attempt to avoid the correlated noise between pixels in inverted images. In each, the lens galaxy is modelled as a singular isothermal ellipsoid, and posterior parameter distributions are sampled using a Markov chain Monte Carlo technique, marginalizing over several sources of residual calibration uncertainty (such as antenna-based phase errors).

Initial lens models were created using the visilens code, which is described in detail elsewhere. The source plane is modelled as one or more elliptical Sérsic profiles. Because of the simplicity of this source-plane representation, the code is able to sample large and complex parameter spaces quickly. The continuum emission at 160 μm, 110 μm and 90 μm was modelled with four Sérsic components, one for SPT0311–58 E and three for SPT0311–58 W. These models leave approximately 8% peak residuals in the 160-μm and 90-μm data, which both reaching peak signal-to-noise ratios of more than 150.

After determining the lens parameters using visilens, we used the best-fitting values as initial input to a pixelated reconstruction code2. This code represents the source plane as an array of pixels, rather than an analytic model, and determines the most probable pixel intensity values for each trial lens model while imposing a gradient-type regularization to avoid over-fitting the data. For each dataset, we fit for the strength of this regularization. At 160 μm and 90 μm we re-fit for the lens model parameters and compare to the visilens models as a test of the robustness of the lens modelling. Within each code, the best-fitting lens parameters at the two independent wavelengths are consistent to within 10%. Further, the lens parameters and the source structure are consistent between the two independent codes, with intrinsic source flux densities, sizes and magnifications that agree to within 15%.

The increased freedom in the source plane afforded by the pixelated reconstruction means that the lens parameters are not independently well constrained by the 110-μm data, which have lower signal-to-noise ratio and spatial resolution. For these data, we apply the lensing deflections determined from the other two datasets to reconstruct the source-plane emission. The pixelated reconstructions of the three continuum wavelengths are shown in Extended Data Fig. 5.

The channelized [C ii] line is modelled using the same pixelated reconstruction technique, using 90 consecutive channels of 40 km s$^{-1}$ width, each with a peak signal-to-noise ratio ranging from 9 to 34. For each channel, we apply the lensing deflections from the best-fitting model of the 160-μm data, which were observed simultaneously. We fit for the strength of the source-plane regularization at each channel, which varies across the line profile as some velocities (those multiply imaged from $-2800 \text{ km s}^{-1}$ to $+800 \text{ km s}^{-1}$) experience higher magnification than others (such as the entire eastern source at $>560 \text{ km s}^{-1}$). The models of each [C ii] channel are represented in Extended Data Fig. 6.

We determined the source magnifications using the 90-μm pixelated model, in which the E source is detected at the highest signal-to-noise ratio and so the effects of varying the aperture used to measure the intrinsic flux density are minimized. Because the source-plane morphology is very similar between the three continuum wavelengths, the magnification is also essentially identical between them.

We find flux-weighted, source-averaged magnifications for the E source, the W source and the system as a whole of $h_{\text{E}} = 1.3$, $h_{\text{W}} = 2.2$ and $h_{\text{sys}} = 2.0$, respectively. These magnifications are substantially lower than the median magnification of 5.5 within the sample of 47 SPT-discovered dusty galaxies for which we have data adequate to construct lens models or to conclude that sources are unlensed. In this case, the lower magnifications result from the effect of gravitational lensing of the halo, which is typically expressed as an ‘Einstein’ radius $\theta_E$. The lens model for this source indicates $\theta_E = 0.29''$, which is around the 10th percentile for SPT lensed sources24, and the background source is both much larger than and offset from the regions of highest magnification. A large portion of the source is therefore only weakly magnified and the source-averaged values are low.

Finally, we also construct a lens model of the 95-GHz ALMA data (rest-frame 380 μm; Extended Data Table 1). Because the spatial resolution of these data are low (3.5″), we model them using only the visilens code, which is more suited to low-resolution data. We allow only the lens parameters and source structural parameters (such as position and radius) to vary within the ranges determined from the higher-resolution 160-μm, 110-μm and 90-μm continuum data, leaving only the flux densities of the E and W sources as free parameters. This modelling indicates that essentially all of the observed 380-μm emission can be ascribed to the W source, with the E source ‘detected’ at about 1σ.
Dust mass. Mass estimates are unmodified from literature values\textsuperscript{43,56,62}, owing to the heterogeneity of the data available across the sample. The dust masses are generally derived from the far-infrared continuum emission, using one to several wavelengths. Differences between the cosmology assumed here and previously result in unimportant corrections and are ignored.

Gas mass. Following standard observational practice, the primary source for the gas mass is the CO line. Without being strongly lensed ($\mu > 1$); erring on the side of overestimating the completeness yields a lower limit on the rareness. Substituting a minimum halo mass of, for example, $10^9 M_\odot$; would make the value of the $\nu$ rareness statistic less than that found for $10^8 M_\odot$; that is, SPT0311–58 would be inferred to be even rarer.

The total area from which the SPT DSFG sample was selected is 2,500 deg$^2$. However, the fact that most of the SPT DSFGs are strongly lensed implies that the effective survey area is potentially much less than 2,500 deg$^2$ because not only must a galaxy have a high intrinsic millimetre-wavelength flux density to be included in the sample but it also must be gravitationally lensed so that it exceeds the approximated 20-ml threshold for inclusion in redshift follow-up observations. Properly accounting for the effects of lensing on the sample completeness would require defining an effective survey area as a function of halo mass and redshift: $A_{\text{eff}}(M_{\text{halo}}) = 2,500 \text{ deg}^2 \times P_{\text{lens}}(M_{\text{halo}})$, where $P_{\text{lens}}(M_{\text{halo}})$ is the probability of a galaxy hosted by a halo of mass $M_{\text{halo}}$ at redshift $z$ being lensed by a factor $\mu_{\text{eff}}$, the minimum magnification necessary for a halo of mass $M_{\text{halo}}$ and redshift $z$ to be detectable. However, given the large uncertainties in determining such a function, we opt for a simpler approach. Instead, in Fig. 3 we plot exclusion curves for the full sky (dotted line), for an area of 2,500 deg$^2$ (dashed line), which corresponds to the assumption that all haloes in the mass and redshift range specified above would be detected even if they were not lensed, and for an area of 25 deg$^2$ (solid line), which corresponds to the assumption that the survey area corresponds to only the approximately 1% of the SPT fields over which the magnification for sources at $z > 1.5$ will be at least $0.027 \mu = 2$, such as SPT0311–58. Code availability. The lensing reconstruction for the ALMA data was initially performed using the visielsen code (https://github.com/jplvisiervisilens). Pixelated reconstructions were performed using a proprietary code developed by a subset of the authors and additional non-authors, and we opt not to release this code in connection with this work. The rareness calculation was performed using publicly available code (https://bitbucket.org/irharrison/hh13-cluster-rareness) that we modified slightly to extend the calculation to $z = 10$. This method enables us to compute $(\zeta, M_{\text{halo}})$ contours (‘exclusion curves’) above which the Poisson probability of such an object being detected in the standard $\Lambda$CDM cosmology is less than $\alpha < 1$; the existence of a single object above such an exclusion curve is sufficient to rule out $\Lambda$CDM at the 100(1−$\alpha$)% confidence level. In Fig. 3, we plot $1\sigma$ exclusion curves ($\alpha = 0.32$). Of the three different statistical measures of rareness proposed\textsuperscript{28}, we use the $>\mu$ measure, which quantifies the rareness according to the minimum height of the primordial density perturbation from which a halo of mass $M_{\text{halo}}$ and redshift $z$ could be formed: $\zeta = \left\langle \chi(z) \cdot \left| P(k) \right| / M_{\text{halo}}(h \sigma) \right\rangle$, where $\chi(z)$ is the normalized linear growth function and $\sigma(M_{\text{halo}})$ is the variance of the matter power spectrum smoothed on the co-moving spatial scale that corresponds to the mass $M_{\text{halo}}$. This statistic is sensitive to changes in the $\Lambda$CDM initial conditions, such as primordial non-Gaussianity (which would lead to more high-mass dark-matter haloes at a given redshift than expected in the standard $\Lambda$CDM cosmology). For the purposes of this calculation, we assume a $\Lambda$CDM cosmology with parameters\textsuperscript{43}$\Omega_{\text{m}} = 0.309$, $\Omega_{\Lambda} = 0.691$, $h_0 = 0.677$ and $\sigma_8 = 0.816$ and use a previously reported halo mass function\textsuperscript{43}.

The $>\mu$ rareness statistic (and the corresponding exclusion curves) depends on the region of the $M_{\text{halo}}-z$ plane to which the survey is sensitive. We assume that the SPT sample of lensed DSFGs is complete for $z > 1.5$. At lower redshift, the probability of lensing is strongly suppressed\textsuperscript{60,62}, which means that the galaxy (or galaxies) associated with a halo mass of more than about $10^{15.5} M_\odot$ (the $M_{\text{halo}}$ value of the exclusion curves for $z = 1.5$) would have to have a very high intrinsic (that is, unladen) millimetre-wavelength flux density (more than about 20 mJy) to be included in the sample. Because of the effects of downsizing (that is, star formation is terminated at higher redshift in higher-mass galaxies than in lower-mass galaxies), it is unlikely that massive galaxies at $z < 1.5$ would have sufficiently high infrared luminosity to be detected by the SPT\textsuperscript{73}. We furthermore assume that the survey is complete for $M_{\text{halo}} > 10^{11} M_\odot$. The assumption that the sample is complete to $M_{\text{halo}} > 10^{11} M_\odot$ is a conservative one because the galaxies hosted by such haloes (which would have $M_{\text{halo}} > 10^{11} M_\odot$) are unlikely to be sufficiently luminous to be detected even if they were not lensed, and for an area of 25 deg$^2$ (solid line), which corresponds to the assumption that the survey area corresponds to only the approximately 1% of the SPT fields over which the magnification for sources at $z > 1.5$ will be at least $0.027 \mu = 2$, such as SPT0311–58.

Data availability. This paper makes use of the following ALMA data: ADS/ JAO.ALMA#2016.1.01293.S and ADS/JAO.ALMA#2015.1.00504.S, available at http://almascience.org/aq?projectcode=2015.1.00504.S and http://almascience.org/aq?projectcode=2016.1.01293.S. The HST data are available online at the Mikulski Archive for Space Telescopes (MAST, https://archive.stsci.edu). Additional data are available online at the proposal ID 14740. Datasets analysed here are available from the corresponding author on reasonable request.

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Extended Data Figure 1 | ALMA continuum images of SPT0311−58.

a–d. Continuum images in ALMA bands 3 (a), 6 (b), 7 (c) and 8 (d), corresponding to rest-frame wavelengths of 380 μm, 160 μm, 110 μm and 90 μm, respectively. Note that the resolution in a is a factor of roughly ten worse than in b–d, and the displayed field of view is also larger by a factor of four. Contours at 10%, 30% and 90% of the image peak in band 6 are shown in a for scale. The ALMA synthesized beam (full-width at half-maximum) is represented as a hatched ellipse in the corner of each image.
Extended Data Figure 2 | Infrared and optical imaging of SPT0311-58. 8\" × 8\" thumbnails of SPT0311-58 in the observed optical and infrared filters are shown. ALMA band 6 continuum contours at 30% and 4% of the image peak are shown in blue; the ALMA synthesized beam is depicted as a blue ellipse in the corner of each image.
Extended Data Figure 3 | Optical, infrared and millimetre-wavelength image of SPT0311−58. The field around SPT0311−58 is shown, as seen with ALMA and HST at 1.3 mm (ALMA band 6; red), 1,300 nm (combined HST/WFC3 F125W and F160W filters; green) and 700 nm (combined HST/ACS F606W and F775W filters; blue). For emission from z = 6.9, no emission should be visible in the ACS filters owing to the opacity of the neutral intergalactic medium, whereas the other filters correspond to rest-frame 160 nm and 160 μm.
Extended Data Figure 4 | De-blending of the optical and infrared images. Left to right, sky image, model and residual images. Top to bottom, HST/WFC3 F125W, Spitzer/IRAC 3.6μm and Spitzer/IRAC 4.5μm data. The ALMA band 6 contours are shown in the left and right columns; the red circles in the right column show the photometric extraction regions for the Spitzer/IRAC images.
Extended Data Figure 5 | Gravitational lensing model of the dust continuum emission in SPT0311−58. For each continuum wavelength for which we have suitable data, we reconstruct the source-plane emission as described in Methods section ‘Gravitational lens modelling’. For each wavelength, from left to right, we show the ‘dirty’ (not de-convolved) image of the data, the dirty image of the model, the model residuals and the source-plane reconstruction. Because the images of the data are not de-convolved, the structure far from the object is due to side lobes in the synthesized beam, and should be reproduced by the models. The image-plane region modelled is evident in the residuals, and results in the ‘noise’ in the source-plane reconstructions. Contours in the residual panels are drawn in steps of $\pm2\sigma$. The lensing caustics are shown in each source-plane panel (ellipse and diamond). The lens parameters are determined independently at 90 $\mu$m and 160 $\mu$m; at 110 $\mu$m we adopt the parameters of the 160-$\mu$m model.
Extended Data Figure 6 | Gravitational lensing model of the [C II] line in SPT0311−58. For each channel (40 km s$^{-1}$ wide), we reconstruct the source-plane emission using the lens parameters determined from fitting to the rest-frame 160-$\mu$m (ALMA band 6) continuum data (Methods section ‘Gravitational lens modelling’). The four images for each channel are as in Extended Data Fig. 5.
Extended Data Figure 7 | Optical to submillimetre-wavelength SED modelling for SPT0311−58 E, SPT0311−58 W and the lens galaxy. The photometric data in Extended Data Tables 2 and 3 for the three components at the position of SPT0311−58 are compared to the models determined using the CIGALE SED modelling code. The lens is modelled assuming a redshift of $z_{\text{phot}} = 1.43$, as estimated with the photometric redshift code EAZY. Upper limits are shown at the 1σ threshold and error bars represent 1σ uncertainties.
Extended Data Table 1 | ALMA observations

| Date       | Frequency (GHz) | Antennas | Resolution (arcsec) | Flux Calibrator | Phase Calibrator | PWV (mm) | t<sub>int</sub> (min) | Noise Level (µJy/beam) |
|------------|-----------------|----------|---------------------|-----------------|------------------|----------|----------------------|------------------------|
| **B3**     |                 |          |                     |                 |                  |          |                      |                        |
| 2016-Jan-02| 91.95           | 41       | 3.8 x 3.9           | Uranus          | J0303-6211       | 1.8      | 1.2                  | 65                     |
| 2015-Dec-28| 95.69           | 34       | 3.2 x 3.5           | Uranus          | J0309-6058       | 2.9      | 1.2                  | 83                     |
| 2015-Dec-28| 99.44           | 34       | 3.1 x 3.4           | Uranus          | J0309-6058       | 2.8      | 1.2                  | 77                     |
| 2015-Dec-28| 103.19          | 34       | 3.0 x 3.4           | Uranus          | J0309-6058       | 2.7      | 1.5                  | 72                     |
| 2015-Dec-28| 106.94          | 34       | 2.9 x 3.3           | Uranus          | J0309-6058       | 2.8      | 1.0                  | 95                     |
| **B6**     |                 |          |                     |                 |                  |          |                      |                        |
| 2016-Nov-03| 233.65          | 45       | 0.25 x 0.30         | J0334-4008      | J0303-6211       | 0.5      | 32.4                 | 24                     |
| **B7**     |                 |          |                     |                 |                  |          |                      |                        |
| 2016-Jun-04| 343.48          | 41       | 0.31 x 0.49         | J2258-2758      | J0303-6211       | 0.8      | 6.5                  | 12                     |
| **B8**     |                 |          |                     |                 |                  |          |                      |                        |
| 2016-Nov-15| 423.63          | 41       | 0.20 x 0.30         |                 |                  | 0.8      | 11.4                 | 53                     |
| 2016-Nov-16| 423.63          | 42       | 0.53 x 0.40         | J0538-4405      | J0253-5441       | 0.5      | 33.7                 |                        |
| 2016-Nov-16| 423.63          | 42       | 0.53 x 0.40         | J0538-4405      | J0253-5441       | 0.5      | 33.7                 |                        |
| 2016-Nov-17| 423.63          | 43       | 0.53 x 0.40         | J0538-4405      | J0253-5441       | 0.3      | 33.7                 |                        |

*a*First local oscillator frequency.

*b*Precipitable water vapour (PWV) at the zenith.

*c*On-source integration time.

*d*Root-mean-square noise level in the 7.5-GHz continuum image.
### Extended Data Table 2 | Optical and infrared photometry

| Telescope | Instrument/Filter | Lens | SPT0311–58E | SPT0311–58W |
|-----------|-------------------|------|-------------|-------------|
| HST       | ACS/F606W         | >27.05 | >28.11   | >27.08   |
| HST       | ACS/F775W         | >26.55 | >27.59   | >26.63   |
| Gemini    | GMOS/i′           | 25.00±0.20 |           |            |
| Gemini    | GMOS/z′           | 24.40±0.20 |           |            |
| HST       | WFC3/F125W        | 23.06±0.16 | 25.28±0.10 | >26.69   |
| HST       | WFC3/F160W        | 22.76±0.15 | 24.98±0.12 | >27.11   |
| Gemini    | FLAMINGOS/Ks 2.16 μm | 22.42±0.13 | ...   | ...   |
| Spitzer   | IRAC/Ch1 3.6 μm   | 21.40±0.14 | 24.47±0.30 | (23.87±0.28) |
| Spitzer   | IRAC/Ch2 4.5 μm   | 21.63±0.13 | 24.45±0.25 | (23.63±0.22) |

All data is given in apparent (not corrected for magnification) AB magnitudes. Limiting magnitudes are reported as 1σ values. The magnification estimates for the E and W sources are 1.3 and 2.1, respectively, as reported in Methods section ‘Gravitational lens modelling’. IRAC photometry for SPT0311–58 W is uncertain owing to blending with the lens, as noted in Methods section ‘Image de-blending’.
Extended Data Table 3 | Far-infrared photometry

| Telescope          | Observed Wavelength | $S_\nu$ (east intrinsic) | $S_\nu$ (west intrinsic) | $S_\nu$ (total apparent) |
|--------------------|---------------------|--------------------------|--------------------------|---------------------------|
| Herschel/SPIRE*    | 250 μm              | 1.9 ± 0.6                | 12.7 ± 4.2               | 29.0 ± 8.0                |
| Herschel/SPIRE*    | 350 μm              | 2.5 ± 0.5                | 16.6 ± 2.9               | 38.0 ± 6.0                |
| Herschel/SPIRE*    | 500 μm              | 3.5 ± 0.6                | 22.7 ± 4.2               | 52.0 ± 8.0                |
| ALMA/B8            | 710 μm              | 3.1 ± 0.2                | 19.9 ± 0.3               |                           |
| ALMA/B7            | 869 μm              | 2.9 ± 0.2                | 15.9 ± 0.25              |                           |
| ALMA/B6            | 1.26 mm             | 1.18 ± 0.05              | 9.77 ± 0.15              |                           |
| ALMA/B3            | 3 mm                | 0.040 ± 0.028            | 0.76 ± 0.02              |                           |

Flux densities ($S_\nu$) are given in mJy.

*Herschel photometry does not spatially resolve the two components; see Methods section ‘Gravitational lens modelling’ for details.