Measurement and ab initio Investigation of Structural, Electronic, Optical, and Mechanical Properties of Sputtered Aluminum Nitride Thin Films

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We report our results on highly textured aluminum nitride (AlN) thin films deposited on glass substrates, oriented along the c-axis, using DC-magnetron sputtering technique for different values of back pressure. The structural, electronic, optical, piezoelectric, dielectric, and elastic properties of sputtered AlN thin films are measured and characterized. In particular, X-ray powder diffraction (XRD) technique shows that AlN thin films exhibit a hexagonal structure. Moreover, we employed ab initio simulations of AlN using the Vienna Ab Initio Simulation Package (VASP) to investigate the structural and the electronic properties of hexagonal AlN structures. The experimental lattice parameters of the as-prepared thin films agree well with those calculated using the total energy minimization approach. The optical parameters of AlN thin films, such as transmittance and refractive index, were measured using UV–vis measurements. Our measurements of refractive index, \( n \), of AlN thin films yield a value of 2.2. Furthermore, the elastic, piezoelectric, and dielectric tensors of AlN crystal are calculated using VASP. The dynamical Born effective charge tensor is reported for all atoms in the unit cell of AlN. Interestingly, ab initio simulations indicate that AlN has a static dielectric constant approximately equal to 4.68, which is in good agreement with the reported experimental value. In addition, the clamped-ion piezoelectric tensor is calculated. The diagonal components of the piezoelectric tensor are found to be \( e_{33} = 1.79 \) C/m\(^2\) and \( e_{31} = -0.80 \) C/m\(^2\). The large values of the piezoelectric coefficients show that a polar AlN crystal exhibits a strong microwave piezoelectric effect. Additionally, the components of the elastic moduli tensor are calculated. The extraordinary electronic, optical, piezoelectric, and elastic properties make AlN thin films potential candidates for several optoelectronic, elastic, dielectric, and piezoelectric applications.

Keywords: AlN thin films, optical, electronic, mechanical, physical tensors, hybrid functional HSE06, DC-magnetron sputtering technique, UV–vis measurements
INTRODUCTION

Aluminum nitride (AlN), in its ground state, crystallizes in a hexagonal close-packed wurtzite structure [1]. AlN thin films have attracted much interest owing to the fact that they have unique features and a wide range of technological applications in various fields such as pressure sensors [2], energy harvesters [3], surface acoustic wave devices [4], and light-emitting devices [5] due to their noticeable large piezoelectric coefficients, $d_{31}$ and $d_{33}$ [6, 7], good electrical isolation [8, 9], wide band gap [10, 11], and high acoustic wave velocity [12, 13]. Additionally, AlN thin films have an exceptional blend of physical, elastic, and chemical properties. AlN exhibits extraordinary optical properties such as large optical band gap energy, ~6.2 eV, and large refractive index, ~2.0. Furthermore, it has interesting electronic, thermal, dielectric, and electronic properties such as extremely high electric resistivity ($10^{14}$ Ω), high thermal conductivity (320 W/m K), large stiffness [14], and high dielectric constant. A bulk of AlN single crystals that are selectively oriented in the c-plane has been synthesized and reported to have a large acoustic wave velocity [15]. The abovementioned interesting properties attracted the attention of several research groups to explore AlN for the fabrication of piezoelectric and optoelectronic devices. Thin films have been grown by several techniques. Methods such as reactive molecular beam epitaxy [16], pulsed laser deposition [17], DC/RF reactive sputtering [18, 19], vacuum arc/cathodic arc deposition [20], ion beam sputtering [21], miscellaneous [22], and sol-gel technique [23] have been implemented to grow AlN thin films of different sizes. The advantage of using reactive sputtering process over the other techniques to synthesize AlN thin films is obtaining films oriented along the c-axis and deposited at room temperature with large piezoelectric coefficients [24, 25].

In this work, we analyze the structural properties of AlN thin films deposited on a glass substrate synthesized by DC-magnetron sputtering technique relative to back pressures. This is an important step to determine the optimum back associated with the equilibrium lattice parameters of AlN thin films. For the sake of comparison, total energy minimization approach embedded in Vienna Ab Initio Simulation Package (VASP) is used to obtain the optimized lattice parameters. We found that the experimental and the calculated lattice parameters are in excellent agreement. Furthermore, we investigate the effect of back pressure on the refractive index and the optical band gap energy of AlN thin films. Theoretically, we present first-principle results on lattice dynamics and the dielectric, piezoelectric, and mechanical properties of AlN to find the interplay between these properties and the potential of this novel material for the current and the next generation of modern devices.

COMPUTATIONAL METHODS AND EXPERIMENTAL PROCEDURE

Experimental Procedure

We prepare AlN thin films of thickness of 550 nm. The as-prepared thin films were deposited on glass substrates. The glass substrate was pre-etched and cleaned in acetone and deionized water in a (Ardenne-LS 730 S) DC-magnetron sputtering machine. A 100-nm Al component of transparency back power on the refractive index and the optical band gap energy of AlN thin films. The Al target and the glass substrate were detached in an ultra-clean deposition chamber evacuated at $1 \times 10^{-5}$ Pa. The deposition chamber contains 100% N\textsubscript{2} gas. The plasma power used was 300 W and the back pressure was set to 0.2, 0.4, or 0.6 Pa.

Computational Methods

Computationally, the density functional theory (DFT)-based self-consistent calculation, with enhanced computational efficiency to predict the ground state of AlN, was used. The gradient of electronic density is a very important parameter in the $ab$ initio calculations; consequently, generalized gradient approximations (GGA) and hybrid functional HSE06 were appropriately implemented in this work [26–30]. For an accurate calculation of the electronic structure, the projector-augmented pseudopotentials (PAW) were used [31–33]. All computations were performed by VASP [34–36]. For the purpose of geometrically optimizing the structure and for total energy minimization, $8 \times 8 \times 5$ k-point mesh was used to sample first the Brillouin zone. The cutoff energy was set to 400 eV. The obtained optimized lattice parameters of AlN were found to be in excellent agreement with previous theoretical and experimental values [37–40]. Although recent $ab$ initio DFT simulations are not successful in predicting the material properties at high temperature, they can still be used to predict accurately the ground state, piezoelectric coefficients, and electronic, optical, and mechanical properties of bulk AlN. Our results are valid up to room temperatures of $T = 300$ K [41–43].

RESULTS AND DISCUSSION

Structural Properties of AlN Thin Film

As shown in Figure 1, AlN crystallizes in a wurtzite hexagonal structure. We investigated the structural properties of AlN thin films computationally and experimentally. Mainly, we implemented DFT-based simulations to obtain the optimized lattice parameters of AlN as well as XRD measurements to investigate the structural properties of the sputtered AlN thin films at a plasma power of 300 W and with different back pressures (0.2, 0.4, and 0.6 Pa) with 100% N\textsubscript{2} atmosphere. Computationally, we relaxed the structure by minimizing the total energy of the unit cell ($i.e.$, as small as $10^{-8}$ eV) and following the Hellmann–Feynman forces that were 0.002 eV/Å at convergence. Minimization of total energy and Hellmann–Feynman forces ensures obtaining highly accurate lattice parameters of AlN structure. The optimization of the lattice parameters of the AlN unit cell is critical for an accurate calculation of the properties of the AlN thin films investigated in this study. We extrapolated the equilibrium in-plane and out-plane lattice parameters $a$ and $c$ of AlN thin film. We found that $a = 3.10$ Å and $c = 4.97$ Å.

Experimentally, the X-ray diffraction (XRD) data obtained using a Cu-K\textsubscript{α} source (wavelength of 0.1540598 nm) X-ray
diffractometer were analyzed to explore the crystallinity of sputtered AlN thin films. Figure 2A shows the XRD pattern of sputtered AlN thin films at a plasma power of 300 W and with different back pressures. The main peaks of the sputtered AlN thin films are observed at Bragg’s as 33.3°, 36.0°, 37.5°, and 42.6° corresponding to the crystallographic planes (100), (002), (101), and (220), respectively. A comparison of observed and standard ‘d’ values of (hkl) planes as matched with Card 01-070-2545 indicates that the AlN thin film is polycrystalline and adopts a wurtzite hexagonal structure [44, 45]. We found that AlN exhibits a polycrystalline structure with a clear (002) orientation. As we increased the back pressure from 0.2 to 0.6 Pa, the (002) peak intensity has increased, indicating a considerable contraction of the corresponding full-width half-maximum (FWHM). More details on the effect of the sputtering conditions on the XRD patterns of textured AlN thin films oriented about the c-axis can be found in Ababneh et al. [24, 25]. The highest peak intensity was found for AlN thin films with (002) orientation. As we increased the back pressure, we observed a considerable increase in the grain size as well as a noticeable improvement of the degree of crystallinity associated with the preferred (002) orientation. Additionally, Figure 2A demonstrates that there is a little shift of all diffraction lines toward the lower diffraction angles (2θ) as the sputtering pressure is increased. The shift in the peaks can be attributed to the sustainable strain in the structure as the sputtering pressure is increased.

Our DFT-based simulations show that AlN exhibits a hexagonal structure that belongs to a space group P6₃mc which has an in-plane lattice constant, \(a\), equal to 3.0977 Å and an out-plane lattice constant \(c = 4.9668 \text{ Å}\). Moreover, the lattice constants \((a)\) and \((c)\) of the hexagonal structure can be calculated from the relation [46, 47]:

\[
\frac{1}{d_{(hkl)}^2} = \frac{4}{3} \left( \frac{h^2 +hk+k^2}{a^2} \right) + \frac{4c^2}{c^2}
\]

where \(d_{(hkl)}\) is the interplanar spacing that can be calculated using Bragg’s law and the angle of incidence \(\theta: \lambda = 2d_{(hkl)} \sin \theta_{hkl}\) [48–52]. From Equation (1) and Bragg’s law, the lattice constants of the wurtzite microstructure of AlN thin films can be evaluated as:

\[
a = \frac{\lambda}{\sqrt{3} \sin \theta_{(100)}}
\]

\[
c = \frac{\lambda}{\sin \theta_{(002)}}
\]

The obtained values of \(a\) and \(c\) of the AlN thin film at a back pressure of 0.2 Pa were found to be 3.104 and 4.995 Å, respectively. As the back pressure increases, the \(a\) and \(c\) slightly increase to 3.109 and 5.021 Å at a back pressure of 0.4 and maintain approximately the same values as the back pressure increases further to 0.6 Pa (as shown in Figures 2B,C). The lattice parameters obtained agree well with the calculated parameters.

The crystalline size, \(D\), can be obtained from Debye Scherrer’s formula as \(D = k\lambda / \beta \cos \theta\) [46, 53], where \(D\) is the crystallite size, \(\beta\) in radians stands for the FWHM, and \(\theta\) and \(k\) represent the Bragg angle and the Scherrer parameter, respectively [54, 55]. Several factors contribute to the lattice microstrain \(\langle \varepsilon \rangle\) such as crystal imperfections, lattice dislocations, and stacking faults [56]. The microstrain of the thin films can be expressed as \(\langle \varepsilon \rangle = \beta \cot \theta \varepsilon\) [53]. The estimated values of the crystallite size, \(D\), and the average microstrain, \(\langle \varepsilon \rangle\), were plotted as functions of sputtering pressure (as shown in Figure 3). At a back pressure of 0.2 Pa, the crystallite size of the AlN thin film was found to be 17.77 nm. However, increasing the back pressure to 0.4 and 0.6 Pa leads to a considerable increase of the crystallite size to 19.579 and 19.578 nm, respectively. It is obvious that increasing the sputtering back pressure would lead to an increase of the degree of crystallinity and in turn to the increase of the crystallite size. This interplay can be interpreted in terms of the formation of larger atomic groups that would lead to an increase in crystallite size. In addition, Figure 3 indicates that, as the back pressure increases, the
microstrain decreases. The opposite trend of the microstrain and the crystallite size could be explained by the fact that, as the volume is occupied by the ordered atoms inside the large atomic crystalline structure, the total surface area increases. This would decrease the shift of plane position and thus reduces the microstrain [57].
Optical and Electronic Characterization of As-prepared AlN Thin Films

Measurement of Index of Refraction and Thickness of AlN Thin Films

A UV–vis spectrophotometer, with a total internal integrating sphere, was employed to investigate the transmittance spectra $T(\lambda)$ of sputtered AlN thin films at 300 W and with different back pressures (0.2, 0.4, and 0.6 Pa) in the spectral range of 250–800 nm. Figure 4 shows the transmittance spectra $T(\lambda)$ of crystalline sputtered as-prepared thin films of AlN. Clearly, the transmittance spectra of the AlN thin films reveal discrete interloping peripheries in the spectral zone of high transparency. This spectral region is characterized by high intensity ($\sim 92\%$). In the short wavelength region, the films begin to absorb the incident light, and consequently the intensity of interloping peripheries begins to decrease and totally vanishes as soon as the absorption edge appears. It was reported that the number of interloping peripheries is basically determined by the thickness of the thin films [58]. The average thin film thickness synthesized has a relatively small value (550 nm); as a result, few observed interloping peripheries are obtained (four fringes only). Furthermore, the appearance of interloping peripheries is an indication of high quality and surface homogeneity of the sputtered AlN thin films. We found that, for wavelength $\lambda < 300$ nm, the transmittance increases rapidly as the wavelength increases. This could be due to the presence of the absorption edge of the AlN thin films and the glass substrate. As illustrated in Figure 4, as the back pressure is increased, the optical transmittance shifts toward a higher-energy region. Therefore, the optical absorption edge is blue-shifted toward a higher energy. This blue-shift is a direct consequence of several factors, mainly the removal of lingering pressures, the improvement of the crystallinity of the sputtered AlN thin films, and the increase in crystallite size [59, 60]. Furthermore, Figure 4 depicts that, at a back pressure of 0.2 Pa, the transmittance spectrum of the sputtered AlN thin films exhibits the lowest value, indicating that the films exhibit the highest index of refraction. Nevertheless, the transmittance of the sputtered AlN thin films at a back pressure of 0.6 Pa exhibits the highest value, indicating that the films exhibit the lowest refractive index. The inset in Figure 4 presents a typical transmittance spectrum, $T(\lambda)$, of sputtered AlN thin films at a back pressure of 0.2 Pa. It also shows two envelopes for
Optical Band Gap Energy, Electronic Density of States, and Band Structure

Tauc plot is commonly used to estimate the band gap energy of semiconductors. It is defined by relating the absorption coefficient with the incident photon energy \((h\nu)\) as \((ah\nu)^{1/n} = \beta(h\nu - E_g)\) [66], where the parameter \(\beta\) indicates band tailing, \(E_g\) stands for optical band gap, and the number \(n\) labels the transition type [67]. The value \((n)\) of crystalline AlN thin films is 1/2 corresponding to the direct allowed transition. Tauc plot has been used by drawing the relationship between the incident energy of the photon \((h\nu)\) in eV vs. \((ah\nu)^2\).

Figure 6 shows the Tauc plot of sputtered AlN thin films at 300 W and with different back pressures (0.2, 0.4, and 0.6 Pa). The band gap of the AlN thin film at 0.2 Pa was found to be 4.51 eV. As sputtering pressure is increased to 0.004 and 0.006 mbar, the band gap energy was found to increase to 4.46 and 4.54 eV, respectively. The reported value of the band gap of AlN is 6.11 eV. The difference between the calculated and the reported values is due to the band gap of the glass substrate.

In order to calculate the electronic band structure of AlN, we employed GGA and hybrid functional HSE06 [68] for exchange correlation potential. Figure 7A depicts the electronic band structure of the AlN thin films. Our results indicate that the AlN thin films exhibit a direct band gap at \(\Gamma\) point, consistent with that of bulk AlN. It is expected that the calculated optical band gap is smaller than the measured value as it is customary for DFT-based \textit{ab initio} electronic simulations to underestimate the value of the optical band gap of metals and semiconductors. One thing to note here is that the first-principle DFT based on GGA suffers from the inevitable gap underestimate [69–71], and this problem may affect the correctness of the calculated band gaps. Therefore, a hybrid functional [68] that evaluates the Fock exchange in real space was introduced. We used the hybrid functional HSE06 to calculate the electronic and the optical properties of AlN. It is expected that the optical band gap obtained using the HSE06 hybrid functional method is more accurate than the one predicted by the GGA method. The band gap energy estimated using the GGA method was found to be 3.72 eV, while the band gap energy estimated using the HSE06 hybrid functional method was found to be 5.07 eV. It can thus be concluded that the calculated values of the band gap energy using HSE06 are more accurate than the values calculated using the GGA method [72–74]. This difference could...
be due to the vacancy’s formation during synthesis and the difference between the experimental and the calculated chemical potentials of the constituents. The electronic properties of AlN can be obtained by executing self-consistent electronic \textit{ab initio} simulations. In particular, electronic density of states (DOS), partial density of states (PDOS), and the electronic band structure are calculated self-consistently [75]. \textbf{Figures 7B,C} display the DOS and the PDOS of AlN thin films using (GGA) and hybrid functional HSE06, respectively. Our results indicate that the bonding between the Al and the N atoms is ionic. Obviously, \textbf{Figures 7B,C} show that there is an expurgated in DOS plot past the Fermi level which designates the optical band gap. The peaks at 3 eV directly above the Fermi level belong to the N electronic state of the conduction band. The DOS and PDOS plots indicate that the states dominating the valence band maximum have energies of $-4.62$, $-4.25$, $-3.53$, $-2.33$, $-1.13$, and $-0.72$ eV below the Fermi level.

\textbf{Optical Dispersions and Optoelectronic Parameters}

Dispersion parameters such as the effective single oscillator ($E_0$), dispersion energy ($E_d$), and static dielectric constant ($\varepsilon_0$) were determined using the Wemple–DiDomenico single effective-oscillator model [53, 76, 77] expressed as:

$$n^2 - 1 = \frac{E_d E_0}{E_0^2 - E^2} \quad (7)$$

By plotting $(n^2 - 1)^{-1}$ vs. $(h\nu)^2$, the dispersion parameters can be evaluated by fitting a straight line. The values of $E_0$ and $E_d$ can then be calculated from the slope $(E_0 E_d)^{-1}$. The values of the dispersion parameters $E_d$ and $E_0$ of the AlN thin films for different values of back pressure are reported in \textbf{Table 1}. Clearly, the $E_0$ value of the AlN thin films increases as the plasma power is increased. The increase of the $E_0$ values of the AlN thin films could be explained as follows: As the plasma power increases, the energy of the bonds between the constituent atoms of the thin film increases, leading to an increase in the values of $E_0$, indicating the sensitivity of this parameter to the bond energy as predicted previously [78]. The obtained values of $E_0$ and $E_d$ are closely related to the $\varepsilon_0$ and the static index of

\begin{table}[h]
\centering
\begin{tabular}{|l|c|c|c|}
\hline
Parameter & 0.2 Pa & 0.4 Pa & 0.6 Pa \\
\hline
Effective single oscillator energy, $E_0$ (eV) & 9.425 & 10.346 & 12.008 \\
Dispersion energy, $E_d$ (eV) & 33.349 & 32.509 & 33.222 \\
Zero-frequency refractive index, $n_0$ & 2.130 & 2.035 & 1.941 \\
Zero-frequency dielectric constant, $\varepsilon_0$ & 4.538 & 4.142 & 3.767 \\
Density of states, $N_c/m^* \times 10^{26}$ (m$^{-3}$kg$^{-1}$) & 6.814 & 4.815 & 2.987 \\
Charge carrier density, $N_c \times 10^{26}$ (m$^{-3}$) & 2.731 & 1.930 & 1.197 \\
High-frequency dielectric constant, $\varepsilon_\infty$ & 4.938 & 4.429 & 3.948 \\
\hline
\end{tabular}
\caption{Estimation of some essential optical parameters of aluminum nitride thin films sputtered at different back pressures.}
\end{table}
refraction $n_0$ as can be deduced from Equation (7) by putting $hv = 0$,

$$
\varepsilon_0 = n_0^2 = 1 + \frac{E_d}{E_0} \quad (8)
$$

The calculated values of $\varepsilon_0$ and $n_0$ of the AlN thin films are presented in Table 1. We found that the values of $n_0$ agree well with the available theoretical and experimental values of the normal index of refraction. The $\varepsilon_0$ and the $n_0$ values of the AlN thin film at 0.5 Pa are found to be 4.54 and 2.13, respectively. We found that, as the back pressure increases to 0.4 and 0.6 Pa, the $\varepsilon_0$ decreases to 4.14 and 3.77, respectively. An accurate measurement of the refractive index is essential to get the free carriers to the effective mass ratio ($N/m^*$) and the frequency-dependent dielectric constant $\varepsilon_\infty$ as comprehended by Fasasi et al. [79] and Spitzer and Fan [80]:

$$
n^2 = \varepsilon_\infty - \frac{1}{4\pi^2\varepsilon_0} \left( \frac{e^2}{c^2} \right) \left( \frac{N_e}{m^*} \right) \lambda^2 \quad (9)
$$

where $e$ is the value of the electronic charge, $N_e$ represents the charge carrier density, $m^*$ is the effective mass of the carrier, and $\varepsilon_\infty$ is the high-frequency dielectric constant. Plotting $n^2$ vs. $\lambda^2$ yields a straight line in the long-wavelength region. The density of states $N/m^*$ is determined from the slope of the straight line. The $\varepsilon_\infty$ parameter can be obtained by extrapolating the straight line to $\lambda^2 = 0$. The values obtained are presented in Table 1. The value of $\varepsilon_\infty$ of the AlN thin film at 0.2 Pa is found to be 4.938. As the back pressure increases, $\varepsilon_\infty$ decreases. Our results provide substantial evidence that the free charge carriers of AlN thin films strongly contribute to their polarization [81, 82].

### Physical Tensors of AlN Thin Films

#### The Static Dielectric Tensor $\varepsilon_0^0$ of AlN

The dielectric properties of AlN were investigated by calculating their response to homogeneous electric fields. We used the density functional perturbation theory [83, 84] to measure the dielectric constants of the thin films. The density functional perturbation theory has been able to precisely investigate the electric field response of the isolated crystal. The static dielectric tensor calculation involves the computation of the electronic and the elastic–piezoelectric response to an external electric field. The static dielectric tensor elements are:

$$
\varepsilon_{ij}^0 = \delta_{ij} + 4\pi \frac{dP_i}{dE_j} \quad (10)
$$

where $E$ and $P$ stand for the electric field and the total macroscopic polarization. The static dielectric tensor and the susceptibility tensor $\chi_{ij}$ defined at vanishing strain are related via $\varepsilon_{ij}^0 = (\delta_{ij} + \chi_{ij})$. The static dielectric tensor can be decomposed into electronic contribution and lattice contribution. We calculated the diagonal components of $\varepsilon_{ij}^0$ of the AlN crystal under the effect of an external field $E = 0.02\delta + 0.02\gamma + 0.02\varphi eV/A$ as presented in Table 2. We found a good agreement between the calculated values of the static dielectric tensor and the experimental values of the zero-frequency dielectric constant measured at 0.2 and 0.4 Pa as can be clearly seen from Table 1. At a higher back pressure of 0.6 Pa, we found that the calculated diagonal elements of static $\varepsilon_{ij}^0$ deviate from the experimental zero-frequency dielectric constant as expected. Our results indicate that, as the back pressure is increased, the discrepancy between the calculated and the experimental $\varepsilon_{ij}^0$ becomes obvious. An accurate calculation of the dielectric constant is fundamental for parameterization of scaled devices. The proper functioning of such scaled devices depends considerably on an appropriate description of the long-wave lattice dynamics [84].

#### Born Effective Charge Tensor of AlN

Investigating the lattice dynamics of the AlN crystal requires an accurate calculation of Born effective charge tensor $Z_{ij}^*$: $\varepsilon_{ij}^0$. The piezoelectric response of the AlN crystal is mainly determined from the interplay of structural fluctuations and the components of $Z_{ij}^*$ tensor of the Al and the N ions. We calculated the $Z_{ij}^*$ tensors of AlN crystal using the density functional perturbation theory and by applying the electric field $E_j$. Accordingly, $Z_{ij}^*$ can be expressed as Alsaad et al. [84]:

$$
Z_{ik}^* = \epsilon \frac{\partial P_i}{\partial u_{ik}} = \epsilon \frac{\partial F_{ik}}{\partial E_j} = -\epsilon \frac{\partial^2 H}{\partial E_j \partial u_{ik}} \quad (11)
$$

where $\partial P_i$ is the polarization induced by the periodic displacement $\partial u_{ik}$ or to the force $F_{ik}$ induced on atom $i$ by the electric field $E_j$. In addition, $Z_{ik}^*$ tensor couples the macroscopic

| TABLE 2 | The electronic contribution to the static dielectric tensor $\varepsilon_{ij}^0$ of aluminum nitride including local field effects (applying external electric field). |
|----------------------|----------------------|----------------------|
| Including local field effects | $\varepsilon_{11}^0$ | $\varepsilon_{22}^0$ | $\varepsilon_{33}^0$ |
|----------------------|----------------------|----------------------|
| 4.627                | 4.626                | 4.687                |

| TABLE 3 | Calculated Born effective charge tensor of aluminum and nitrogen ions of aluminum nitride calculated by applying a homogenous electric field $E = 0.02\delta + 0.02\gamma + 0.02\varphi eV/A$. |
|----------------------|----------------------|----------------------|
| Atomic species | $Z_{xx}$ | $Z_{xy}$ | $Z_{xz}$ | $Z_{yy}$ | $Z_{yz}$ | $Z_{zx}$ | $Z_{zy}$ | $Z_{zz}$ |
|----------------------|----------------------|----------------------|
| Al$_1$ | 2.50 | 0.00 | 0.00 | -0.00 | 2.50 | -0.00 | -0.00 | 0.00 | 2.67 |
| Al$_2$ | 2.50 | -0.00 | -0.00 | -0.00 | 2.50 | 0.00 | 0.00 | -0.00 | 2.67 |
| N$_3$ | -2.56 | 0.00 | 0.00 | 0.00 | -2.56 | -0.00 | -0.00 | 0.00 | -2.66 |
| N$_4$ | -2.56 | 0.00 | -0.00 | 0.00 | -2.56 | 0.00 | 0.00 | -0.00 | -2.66 |

| TABLE 4 | The piezoelectric tensor components $e_{ij}$ of aluminum nitride (in C/m$^2$). |
|----------------------|----------------------|----------------------|
| Phase | $e_{16}^0$ | $e_{16}^0$ | $e_{25}^0$ | $e_{26}^0$ | $e_{31}^0$ | $e_{32}^0$ | $e_{33}^0$ | $e_{34}^0$ |
|----------------------|----------------------|----------------------|
| P2i (c) | -0.00 | -0.60 | -0.59 | -0.00 | -0.80 | -0.80 | 1.78 | -0.00 |
polarization $P_j$ and periodic atomic displacements via:

$$P_j = \frac{e}{V} \sum Z_{ijk}^* \delta u_{ij,k}$$  \hspace{1cm} (12)$$

where $i$ denotes the $i^{th}$ atom and $j$ and $k$ are the directions of the polarization component and the atomic displacement, respectively. The $Z_{ijk}^*$ tensor of the Al and the N ions of the AlN crystal was calculated from the response to a homogenous electric field. Our results are in good agreement with the previous results [85, 86].

Table 3 indicates that the acoustic-sum rule [87] that examines the charge neutrality is satisfied. For every direction $i$ and $j$, one must have $\sum_k Z_{k,ij}^* = 0$ [88]. As can be seen from Table 3, the $Z_{k,ij}^*$ of the Al atoms covalently bonded to the nitrogen atom is positive and effectively creates a local dipole moment with the negatively charged nitrogen atoms.

The Piezoelectric Tensor of AlN Thin Films

Wurtzite piezoelectric materials have about two orders of magnitude lesser piezo-response compared to Perovskite materials. However, materials like wurtzite AlN can maintain a hysteresis-free behavior, with high-temperature thermal stability and easier production techniques. The piezoelectric stress coefficient ($\varepsilon_{ijk}$) can be expressed as Duerloo et al. [89]:

$$\varepsilon_{ijk} = \frac{dP_i}{dn_{jk}} = \frac{d\sigma_{jk}}{dE_i}$$  \hspace{1cm} (13)$$

The piezoelectric coefficient can be decomposed into a clamped-ion part ($\varepsilon_{ij}^{(0)}$) and an internal-strain part ($\varepsilon_{ij}^{(int)}$), i.e., $\varepsilon_{ij} = \varepsilon_{ij}^{(0)} + \varepsilon_{ij}^{(int)}$ [90, 91]. In principle, the clamped-ion piezoelectric coefficient can be defined as Alsaad et al. [84]:

$$\varepsilon_{ij}^{(0)} = - \frac{\partial \sigma_i}{\partial E_j} \quad i = xx, yy, zz, xy, yz, zx \quad and \quad j = x, y, z,$$  \hspace{1cm} (14)$$

FIGURE 8 | (A) 3D plot, (B) xy 2D plot, (C) yz 2D plot, and (D) the magnitude of the largest value of the piezoelectric tensor of aluminum nitride crystal.
In terms of energy per undeformed unit volume, the clamped-ion piezoelectric tensors can be written as:

$$\varepsilon_{ij}^{(0)} = -\frac{\partial^2 H}{\partial E_i \partial \eta_j} |u$$

and the internal-strain piezoelectric coefficient as:

$$\varepsilon_{ij}^{(int)} = -\frac{\partial^2 H}{\partial E_i \partial \eta_j} |\eta$$

In Table 4 is a list of the calculated clamped-ion piezoelectric coefficient $\varepsilon_{ij}^{(0)}$ tensor for wurtzite AlN. The coefficients $\varepsilon_{33}^{(0)}$ and $\varepsilon_{31}^{(0)}$ which represent the induced polarization produced along the z-direction as uniaxial strain $\eta_{33}$ and shear strain $\eta_{31}$ are applied. The uniaxial strain $\eta_{33}$ twists the Al–N bond, causing the polarization vector to rotate along the z-direction, producing a large change in the electric dipole as clearly demonstrated in Figures 8A–C that show the 3D and the 2D plots of the piezoelectric tensor of AlN. Figure 8D shows the default plot of the magnitude, indicating along which direction the polarization is the largest.

Internal Stain Tensors of AlN

It is customary to define the force–response internal strain tensor as Alsaad et al. [84]:

$$\lambda_{mj} = -V \frac{\partial^2 H}{\partial u_m \partial \eta_j} |E$$

Usually, crystals with basis contain one or more atoms that subjugate sites lacking inversion symmetry and which exhibit considerable internal strain tensors. Table 5 shows the internal strain tensor of the displaced atoms of Al and N atoms. The computation of internal strain tensors is crucial for the determination of the different inner elastic constants of the AlN crystal. Thus, theoretically, they provide a deeper insight into understanding the structure and bonding. Practically, they are essential for tracking atomic displacements in a homogeneously stressed crystal and consequently are relevant to the elucidation of the properties of crystals that are explored under conditions of precisely defined stress.

The Elastic Stiffness Tensor of AlN Thin Films

A deep understanding of the elastic properties of AlN could be useful for potential applications of AlN in flexible electronic devices. The elastic stiffness of AlN has a symmetric form. It is an inherited feature of the space group $P6_3mc$ to which AlN belongs.

The calculated elements of the elastic moduli are presented in Table 6. Figures 9A–C show the two- and three-dimensional surface constructions of the elastic modulus of AlN. It is obvious that the elastic modulus of AlN exhibits an apparent deviation in shape from spherical symmetry, indicating a strong anisotropic behavior along different symmetrical directions. The 3D contour deviates from the spherical shape laterally along the z-axis, along which it exhibits the largest value. The large deviation from the spherical shape along the z-axis indicates that the elastic modulus of AlN is highly anisotropic. Figure 9D shows the default plot of the magnitude of the elastic constant, indicating that AlN exhibits the maximum value along the z-direction.

We parameterized the elastic stiffness tensor of AlN. We found it to be symmetrical $\lambda_{ij} = \lambda_{ji}$ as illustrated in Table 6, confirming that the elastic tensor is isotropic. The table shows that AlN exhibits negative diagonal elastic moduli, and the magnitudes of the components indicate that the material is relatively soft. This result shows that this material has a potential to be used in flex circuits for flexible electronic applications [94]. A sophisticated electronic skin that senses pressure pulses demonstrated on an integrated display of organic.

| TABLE 5 | Internal strain tensor (Voigt notation) of Al1, Al2, N1, and N2 for displacements in x, y, and z (\$/\text{m}) | | | | | |
| Index | 1 | 2 | 3 | 4 | 5 | 6 |
| Al1 | | | | | | |
| 1 | −0.00 | −0.02 | −0.00 | −7.04 | −0.00 | −4.43 |
| 2 | −7.22 | 7.23 | 0.00 | 0.33 | −4.20 | −0.00 |
| 3 | −4.72 | −4.73 | 10.6 | −0.00 | 0.00 | −0.00 |
| Al2 | | | | | | |
| 1 | −0.00 | −0.02 | −0.00 | −7.04 | −0.00 | −4.43 |
| 2 | −7.22 | 7.23 | 0.00 | 0.33 | −4.20 | −0.00 |
| 3 | −4.72 | −4.73 | 10.6 | −0.00 | 0.00 | −0.00 |
| N1 | | | | | | |
| 1 | −0.00 | −0.02 | −0.00 | −9.08 | 0.00 | 4.51 |
| 2 | −9.11 | 9.13 | 0.00 | 0.07 | 4.58 | 0.00 |
| 3 | 4.70 | 4.70 | −10.5 | 0.00 | 0.00 | −0.00 |
| N2 | | | | | | |
| 1 | −0.00 | −0.02 | −0.00 | −9.08 | 0.00 | 4.51 |
| 2 | −9.11 | 9.13 | 0.00 | 0.07 | 4.58 | 0.00 |
| 3 | 4.70 | 4.70 | −10.5 | 0.00 | 0.00 | −0.00 |

| TABLE 6 | Elastic moduli $\lambda_{ij}$ at constant electric field $E$ of aluminum nitride crystal (kbar) | | | | | |
| Direction | 1 | 2 | 3 | 4 | 5 | 6 |
| Direction | 1 | 2 | 3 | 4 | 5 | 6 |
| 1 | −552.94 | 271.62 | 315.34 | 5.18 | 0 | 0 |
| 2 | 271.62 | −554.51 | 315.07 | −6.48 | 0 | 0 |
| 3 | 315.34 | 315.07 | −704.40 | −0.238 | 0 | 0 |
| 4 | 5.18 | −6.48 | −0.238 | −408.99 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | −102.79 | −0.1636 |
| 6 | 0 | 0 | 0 | 0 | −0.1636 | −106.89 |
light-emitting diodes has been reported [95–104]. We found that AlN exhibits Young's modulus of 302 GPa and shear modulus of 126 GPa, along with its light weight and non-toxic nature, making it eligible as a substrate for flex circuit boards and electronic skin.

**CONCLUSION**

In summary, piezoelectric aluminum nitride thin films were synthesized by reactive DC-magnetron sputtering on a glass substrate with different back pressures. The optimization process was performed to obtain highly textured thin films with enhanced piezoelectric response via studying the interplay between the microstructure and the electronic, optical, piezoelectric, and dielectric properties. X-ray powder diffraction was used to investigate the structural properties. The XRD measurements confirm that the AlN thin films exhibit a hexagonal structure. The dominant crystallographic orientation is found to be (002) plane with the optimum intensity in comparison with other possible orientations. VASP based on density functional theory and generalized gradient approximation was used to investigate the structural and the electronic properties of hexagonal AlN structures. The experimental and the theoretical optimized lattice parameters of AlN were found to be in good agreement. The optical properties of sputtered AlN thin films at different back pressures were investigated by performing UV–vis spectrophotometer measurements of their
transmittance spectra. The refractive index and the optical band gap of the sputtered AlN thin films were calculated accordingly. The refractive index of the AlN thin films was found to be 2.15. We found that the measured optical band gap of the AlN thin film (4.5 eV) is higher than the \( ab \) \( initio \) calculated value that is found to be 3.85 eV, consistent with the previously reported calculated value. This discrepancy is expected as it is well known that first-principle techniques underestimate the optical band gap considerably. In addition, the elastic, piezoelectric, and dielectric tensors of AlN crystal were calculated by employing VASP within the framework of DFT. The dynamical Born effective charge tensor of the AlN system that is crucial for lattice dynamical investigations was reported for all atoms in the unit cell. The value of the principal component of electronic contribution to the static dielectric tensor of AlN was found to be \( \approx 4.68 \). Furthermore, clamped-ion piezoelectric tensor was calculated. The diagonal components were found to be \( e_{33} = 1.784 \) and \( e_{31} = -0.80 \) \( C/m^2 \), demonstrating a reasonable piezoelectric response of this polar crystal. The interplay between the structural, electronic, optical, elastic, and piezoelectric properties of the polar AlN crystal indicates a potential attractive perspective for cheap and efficient optoelectronic, piezoelectric, and mechanical applications. Based on our results, AlN films are promising for communication systems, electromechanical, dielectric, and piezoelectric applications, and information storage devices.

**DATA AVAILABILITY STATEMENT**

The datasets generated for this study are available on request to the corresponding author.

**AUTHOR CONTRIBUTIONS**

AMA, QA-B, IQ, AAA, AA, ZA, IA, and AT: measurements of physical tensors and elastic properties, data analysis and acquisition, and editing the manuscript.

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