Sulfur and zinc abundances of red giant stars

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Abstract

Sulfur and zinc are chemically volatile elements, which play significant roles as depletion-free tracers in studying galactic chemical evolution. However, regarding red giants having evolved off the main sequence, reliable abundance determinations of S and Zn seem to be difficult despite that a few studies have been reported so far. Given this situation, we tried to establish the abundances of these elements for an extensive sample of 239 field GK giants (−0.8 \(\lesssim\) [Fe/H] \(\lesssim\) +0.2), by applying the spectrum-fitting technique to S i 8694–5, S i 6757, and Zn i 6362 lines and by taking into account the non-LTE effect. Besides, similar abundance analysis was done for 160 FGK dwarfs to be used for comparison. The non-LTE corrections for the S and Zn abundances derived from these lines turned out \(\lesssim\) 0.1(−0.2) dex for most cases and not very significant. It revealed that the S i 6757 feature is more reliable as an abundance indicator than S i 8694–5 for the case of red giants, because the latter suffers blending of unidentified lines. The finally resulting [S/Fe]–[Fe/H] and [Zn/Fe]–[Fe/H] relations for GK giants were confirmed to be in good agreement with those for FGK dwarfs, indicating that S and Zn abundances of red giants are reliably determinable from the S i 6757 and Zn 6362 lines. Accordingly, not only main-sequence stars but also evolved red giant stars are usable for tracing the chemical evolution history of S and Zn in the regime of disk metallicity by using these lines.

Key words: stars: abundances — stars: atmospheres — stars: evolution — stars: late-type

* Based on data collected at Okayama Astrophysical Observatory of NAOJ (Okayama, Japan).
1. Introduction

Sulfur and zinc are counted as important elements in stellar spectroscopy. Owing to their “volatile” characteristics, they are hardly affected by condensation processes (unlike refractory elements such as Fe, which may suffer gas–dust depletion). For this reason, S (α group) and Zn (Fe-group element) are regarded to play significant roles in galactic chemical evolution, since they may be used as depletion-independent tracers of nucleosynthesis history. Accordingly, not a few spectroscopic investigations on the behavior of [S/Fe] and [Zn/Fe] in stars of various metallicities have been done toward clarifying the chemical enrichment history of these elements in the Galaxy (see, e.g., Takada-Hidai et al. 2005 for S, Caffau et al. 2005 for S, Saito et al. 2009 for Zn, Takeda et al. 2005c for S and Zn, and the references therein).

However, regarding stars of Galactic disk population, unevolved dwarfs of F–G type have been primarily used for such studies of S and Zn abundances, while few reliable abundance results of these elements are available for red giants (evolved low–to-intermediate-mass stars), despite that several extensive abundance studies on a large sample of field giants have been reported in the past decade:

— S and Zn were out of the target elements in Takeda, Sato, and Murata’s (2008; hereinafter referred to as Paper I) analysis for 322 G–K giants due to the limited wavelength range of the spectra.

— In Luck and Heiter’s (2007) spectroscopic study of 298 field giants, S and Zn abundances were determined only for 10 and 6 stars, respectively, which were not sufficient for establishing the trends of [S/Fe] or [Zn/Fe].

— Luck (2015) recently reported the abundance results for a very extensive sample of 1133 field G–K giants. While S and Zn abundances were determined for most stars, the dispersions of [Element/Fe] ratios are unusually large (≈±0.4 dex) only for these two elements (cf. Figure 5 therein), which means that they are unreliable. Actually, as noted by Luck (2015) himself, [S/Fe] systematically grows from ≈0 (T_{\text{eff}} ≈5500 K) to ≈2 (T_{\text{eff}} ≈4000 K), manifestly indicating an involvement of appreciable blending (with unknown lines) becoming progressively important toward later spectral types (see Figure 6 therein). Regarding Zn, Luck (2015) similarly remarked that “The zinc lines are badly blended, especially at temperatures below 4800K, resulting in abundances of poor quality.”

— Very recently, Maldonado and Villaver (2016) published the abundances of 16 elements (including S and Zn) for a large sample of evolved stars and compared those of unevolved main-sequence stars. As seen from their Fig. A.1, [S/Fe] results for evolved stars are systematically higher than those for main-sequence stars, and the dispersion of [Zn/Fe] for giants is appreciably larger than that for dwarfs, which implies that larger errors may be involved in their abundances of these elements for red giants.

— In Jofré et al.’s (2015) comparison of their abundance results for giant stars with literature
studies (cf. Fig. 7 therein), Zn abundances were compared with those of Maldonado, Villaver, and Eiroa (2013); but the consistency was not necessarily satisfactory.

It is thus evident that abundance studies of these two elements for evolved red giant stars are still at quite unsatisfactory level, which are yet to be conducted by a careful analysis of appropriate spectral lines. Takeda et al. (2015; hereinafter referred to as Paper II) investigated the oxygen abundances (along with those of C and Na) for 239 late G and early K giants by using the $R$- and $I$-band spectra (up to $\sim 8800 \, \text{Å}$) newly obtained in the 2012–2013 period. This was originally intended to supplement/revise the previous work of Paper I, which was based on old spectra covering only the yellow–orange region ($\sim 5000–6200 \, \text{Å}$). Since these new longer-wavelength region spectra comprises important spectral lines usable for determinations of S and Zn abundances ($\text{S} \, \text{i} \, 8693–5$, $\text{S} \, \text{i} \, 6757$, and $\text{Zn} \, \text{i} \, 6362$), we decided to make use these data and determine the S and Zn abundances of 239 red giants by using the spectrum-fitting method while properly including the non-LTE effect.

Accordingly, we would like to examine in this investigation whether abundances of S and Zn can be reliably determined for low-gravity giants of G–K type. Toward this purpose, the S and Zn abundances of unevolved 160 dwarfs (including subgiants) of late-F through early-K type were also derived in essentially the same manner, which we intend to use as reference samples for comparing the abundance trends. That is, given that both S and Zn should not suffer any surface abundance change (unlike the abundances of some light elements such as Li or C, which are affected by evolution-induced mixing of nuclear-processed materials), we may expect that essentially the same $[\text{S}/\text{Fe}]–[\text{Fe}/\text{H}]$ or $[\text{Zn}/\text{Fe}]–[\text{Fe}/\text{H}]$ relation would be obtained for both GK giants and FGK dwarfs. If such a consistency could be confirmed, we may state that trustworthy abundances of these elements are established also for giants.

Since abundance studies of two samples (GK giants and FGK dwarfs) are involved in this investigation based on different data sets by making use of our previous results, we firstly outline the adopted observational data, the atmospheric parameters, and the method of line-strength measurement (to be described in section 2 and section 3) in table 1 for the reader’s convenience.

The remainder of this article is organized as follows: The abundance determination procedures (spectrum-fitting analysis, equivalent-width derivation, and derivation of non-LTE abundances) for our 239 program stars of GK giants are described in section 2. Section 3 is devoted to a brief description of S and Zn abundances for the reference sample of 160 FGK dwarfs. The resulting abundances along with the related quantities are discussed in section 4, where the $[\text{Fe}/\text{H}]$-dependent trends for giants and dwarfs are compared with each other. The conclusions are summarized in section 5.
2. S and Zn abundances of GK giants

The high-dispersion spectra of 239 G–K giants used for this study are the same as adopted in Paper II (see section 2 therein), which were obtained in 2012–2013 by using the HIDES at the coudé focus of the 188 cm reflector at Okayama Astrophysical Observatory. Regarding the atmospheric parameters [the effective temperature ($T_{\text{eff}}$), surface gravity ($\log g$), Fe abundance relative to the Sun ([Fe/H]), and microturbulence ($v_t$)], we exclusively adopted those spectroscopically determined in Paper I unchanged (cf. subsection 3.1 therein). The atmospheric model of each star corresponding to these parameters was generated by interpolating Kurucz’s (1993) ATLAS9 model grid as in Paper I.

Our abundance determination closely follows the procedure adopted in Paper II (see section 3 therein for more details), which consists of three consecutive steps: (i) synthetic spectrum fitting to derive provisional abundances for the important elements in the relevant spectrum range, (ii) inverse calculation of the equivalent width for the line (or the blended feature) of S or Zn in question by using the fitting-based abundance solutions, and (iii) analysis of such established equivalent widths to derive the final abundances or abundance errors due to uncertainties in atmospheric parameters.

Given that new $R$- and $I$-band spectra (up to $\sim 8800$ Å) are available for our targets, we selected three wavelength regions for abundance determinations of S and Zn: (a) 8691–8696 Å region comprising the S i 8693–5 triplet lines (along with Ti i 8692.33 and Nd ii 8685.17), (b) 6756–6758.1 Å region comprising the blended feature of S i 6757 lines (along with Fe i 6756.56 and Co i 6757.71, and (c) 6362–6365 Å region comprising the Zn i 6362.34 line (along with [O i] + CN 6363 feature) which we already analyzed in Paper II for oxygen abundance determination. The adopted atomic data of the relevant S and Zn lines are summarized in table 2.

The convergence of the fitting solutions turned out fairly successful for most of the cases. How the theoretical spectrum for the converged solutions fits well with the observed spectrum for each of the 239 GK giants is displayed in figure 1 (8691–8696 Å fitting, where S, Ti, and Nd abundances were varied) and figure 2 (6756–6758.1 Å fitting, where S, Fe, and Co abundances were varied). See Fig. 4 in Paper II for the case of 6362-6365 Å fitting where O, Fe, Zn, and CN abundances were varied.

Then, based on these fitting-based abundances, we computed the equivalent widths for the S i 8694.63 line ($W_{8695}$; the strongest component of the triplet), the S i 6757 feature ($W_{6757}$; comprising three components), and the Zn i 6362.34 line ($W_{6362}$), from which the

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1 Regarding the atomic data of other spectral lines included in these spectral ranges, which are needed for spectrum synthesis calculations, we basically adopted Kurucz and Bell’s (1995) compilation. However, we applied rough corrections to the original log $gf$ values given therein for the following lines, in order to accomplish a better fit: Nd ii 8695.170 (by +1.0 dex), Ni i 6757.714 (by +1.0 dex), Si i 6758.005 (by −1.0 dex; i.e., reduced to a negligible level), and Ni i 6758.061 (by −1.0 dex; i.e., reduced to a negligible level).
non-LTE abundances \((A)\)^2 and the relevant non-LTE corrections \((\Delta)\) were derived, where the non-LTE effect for S and Zn lines was taken into account based on the grid of non-LTE departure coefficients calculated by Takeda et al. (2005c) with the standard treatment of H i collision cross section (i.e., \(h = 0\)). The resulting equivalent widths and non-LTE abundances as well as corrections for the 239 giants are given in tableE1.txt (on-line material).

In order to estimate abundance errors due to ambiguities in atmospheric parameters, we computed the changes in the S and Zn abundances while perturbing the standard atmospheric parameters interchangeably by \(\pm 100\) K in \(T_{\text{eff}}\), \(\pm 0.2\) dex in \(\log g\), and \(\pm 0.2\) km s\(^{-1}\) in \(\xi\), as done in Paper II. The mean values of the resulting abundance changes averaged over 239 stars are summarized in table 3. We can see from this table that the typical extents of such uncertainties are within \(\lesssim 0.1\) dex and thus not so significant.

3. Comparison sample of FGK dwarfs

Regarding the S and Zn abundances of 160 FGK dwarfs (including some subgiants), with which the abundance results of 239 giants are to be compared, essentially the same determination procedures as described in section 2 (i.e., non-LTE analysis of \(W_{8695}\), \(W_{6757}\), and \(W_{6362}\)) were adopted. Our analysis closely follows Takeda’s (2007) study, which is based on the spectra published by Takeda et al. (2005a) along with the atmospheric parameters determined by Takeda et al. (2005b).

The \(W_{8695}\) data (for S i 8694.63) were inversely derived by using the solutions of 8692.5–8695.5 Å fitting done by Takeda (2007; cf. Fig. 4 therein), while Takeda’s (2007) directly measured \(W_{6362}\) data were used for Zn i 6362.34. As to the S i 6757 line feature which was not analyzed by Takeda (2007), we newly carried out a spectrum-fitting analysis in the 6756–6758.1 Å region and computed \(W_{6757}\) for each star (as done for giants). Figure 3 shows how the fitting between the observed and theoretical spectra has been accomplished for each of the 160 targets.

The equivalent widths and the resulting non-LTE abundances as well as corrections for these 160 dwarfs(+subgiants) are presented in tableE2.txt (on-line material).

4. Results and discussion

4.1. Behaviors of abundances and related quantities

We now examine the abundances as well as the related quantities resulting from our analysis described in section 2 (giants) and section 3 (dwarfs).

The strengths of S i 8695, S i 6757, and Zn i 6362 lines \((W_{8695}, W_{6757}, \text{and } W_{6362})\) are

\[A\] We use \(A\) to denote the logarithmic elemental abundance (often expressed as \(\log \epsilon\)) relative to hydrogen. That is, if number density in the atmosphere for element X and H is \(N(X)\) and \(N(H)\), respectively, \(A(X)\) is defined as \(A(X) \equiv \log N(X) - \log N(H) + 12\).
plotted against $T_{\text{eff}}$ and $\log g$ in figure 4, where how the non-LTE corrections ($\Delta$) depend upon $W$ is also shown. We can recognize a tendency that S I lines tend to be strengthened with an increase in $T_{\text{eff}}$ or with a decrease in $\log g$, while such a trend is not clear for the case of Zn I 6362 line in dwarfs. The non-LTE corrections are negative ($\Delta < 0$) for most cases (except for the Zn I 6362 line for dwarfs, where $\Delta$ tends to become positive at the weak-line limit; cf. figure 4i) and their extents ($|\Delta|$) show a tight correlation with $W$ (increasing with an increase in $W$). Besides, since the non-LTE effect is enhanced in the condition of lower gravity (lower density), the $|\Delta|$ values for giants are larger than those for dwarfs (when compared at the same $W$). Generally speaking, the non-LTE corrections are $\lesssim 0.1$ dex for most cases (for all cases of S I 6757 and Zn I 6362) and not very significant, except for the case of especially stronger S I 8695 line corresponding to higher-luminosity giants of $\log g \lesssim 2$ where $|\Delta|$ becomes as large as $\sim 0.2$–0.3 dex (cf. figure 4g).

Each of the non-LTE abundances $[A(S)_{8695}, A(S)_{6757}, \text{ and } A(Zn)_{6362}]$ are plotted against $T_{\text{eff}}$ and $\log g$ in figure 5, where $A(S)_{8695}$ vs. $A(S)_{6757}$ correlations for giants and dwarfs are also shown. We can see that the S abundances derived from S I 8695 and S I 6757 lines are fairly good agreement for dwarfs (figure 5h) but not for giants (figure 5g); i.e., the scatter is rather large and $A(S)_{8695}$ tends to be systematically larger than $A(S)_{6757}$ in the regime of high $A(S)$. Regarding giants, we can recognize that the fit for S I 8693–5 lines (figure 2) is apparently not so good as for S I 6757 feature (figure 3). This suggests that blending effect due to other lines (not included in our analysis; e.g., molecular lines) may possibly take effect for the former S I 8693–5 case especially at lower $T_{\text{eff}}$ and higher [Fe/H], making $A(S)_{8695}$ more or less overestimated. Actually, a signature of overestimation for $A(S)_{8695}$ is also observed in the maximum abundance ($A_{\text{max}}$) among the sample. Since $[\text{Fe/H}]_{\text{max}}$ is $\sim +0.4$–0.5 for dwarfs (Takeda 2007) and $\sim +0.2$ for giants (Paper I), similar difference should be observed also for $A_{\text{max}}$ between dwarfs and giants. While such a discordance amounting 0.2–0.3 dex is surely recognized in $A(S)_{6757}$ (figure 5e) and $A(Zn)_{6362}$ (figure 5f), we can not detect any difference in the maximum values of $A(S)_{8695}$ between dwarfs and giants in figure 5d, which implies that $A(S)_{8695}$ values of giants are likely to be overestimated at the high-metallicity regime (presumably due to appreciable blending effect). Accordingly, we may state that S abundances derived from S I 6757 are more reliable than those from S I 8695 as far as red giants are concerned, because the latter is more vulnerable to blending effects resulting in appreciable overestimation.

This consequence is further substantiated by figure 6, where the resulting values of $W$, $\Delta$, and $[X/\text{Fe}]$ (X is S or Zn) for each line are plotted against [Fe/H] (metallicity). We can see that $[S/\text{Fe}]$ vs. [Fe/H] relation for 239 giants constructed from $A(S)_{8695}$ (filled symbols in

\[ [X/\text{Fe}] = [X/\text{H}] - [\text{Fe/H}] = [A_\star(X) - A_\odot(X)] - [A_\star(\text{Fe}) - A_\odot(\text{Fe})], \]

where $A(X)$ is the non-LTE abundance derived in this study and [Fe/H] is the Fe abundance relative to the Sun determined in Paper I (giants) and Takeda et al. (2005b) (dwarfs). Here, the subscripts $\star$ and $\odot$ denote “star” and “Sun”, respectively.
figure 6g) is appreciably different from that constructed based on \( A(S)_{6757} \) (filled symbols in figure 6h) in the sense that the former shows a significantly larger scatter than the latter. This manifestly indicates that \( A(S)_{8695} \) is less reliable than \( A(S)_{6757} \) and thus should not be used for the case of red giants.\(^4\) Hereinafter we will exclusively adopt \( A(S)_{6757} \) as the final sulfur abundances for both giants and dwarfs. According to figure 6h and figure 6i, both giants (filled symbols) and dwarfs (open symbols) appear to follow almost the same (and reasonably tight) \([S/Fe] \) vs. \([Fe/H] \) (from S \( \lambda 6757 \)) and \([Zn/Fe] \) vs. \([Fe/H] \) (from Zn \( \lambda 6362 \)) relations. We will actually confirm this fact in subsection 4.3.

4.2. Comparison of S and Zn abundances for giants with published results

The \([S/H] \) and \([Zn/H] \) values (differential S or Zn abundances relative to the Sun) for giants derived in this study are compared with the literature results in figure 7.

Regarding sulfur, all the \([S/H] \) values published by Luck (2015), Luck & Wepfer (1995), and Maldonado & Villaver (2016) tend to be systematically larger (typically by several tenths dex) than our \([S/H] \) derived from S \( \lambda 6757 \), as shown in figure 7a, figure 7c, and figure 7e, respectively. Although Luck (2015) as well as Luck and Wepfer (1995) did not explicitly describe the lines employed for their S abundance determination, we presume that they used any of the S \( \lambda 8670.200, 8670.627, 8671.308, 8678.950, 8680.445, 8693.150, 8693.958, \) and 8694.641 lines, as inferred from the line list presented in Luck and Lambert (1985; cf. Table 1 therein). It is thus likely that they derived overestimated S abundances, because near-infrared (I-band) lines tend to suffer blending effect as we confirmed for S \( \lambda 8693–5 \) lines. Meanwhile, Maldonado and Villaver (2016) used S \( \lambda 6046.00, 6052.66, \) and 6757.17 lines as included in Table 3 of Maldonado et al. (2015). While S \( \lambda 6757 \) line among these is the same as we adopted, the other two S \( \lambda 6046/6052 \) lines may have suffered some appreciable blending with unknown lines. In any case, since equivalent-width data of the adopted lines are not published in these three literature studies, we can not trace down the true reason for this discrepancy.

As to zinc, we compared our \([Z/H] \) results with those of five previous studies in figure 7. It can be seen from figure 7b, figure 7d, and figure 7g that Luck (2015), Luck & Wepfer (1995), and Jofrè et al. (2015) yielded systematically larger \([Zn/H] \) values (by several tenths dex) than our results. The adopted Zn line is again not explicitly stated in the former two papers (though we presume they employed Zn \( \lambda 6362 \) line), while Jofrè et al. (2015) used Zn \( \lambda 4722.16 \) and \( \lambda 4723.16 \) for their zinc abundance determination.

\(^4\) Actually, this argument applies not only to giants but also to dwarfs, since the dispersion of \([S/Fe]_{8695} \) (figure 6g) appears to be larger than that for \([S/Fe]_{6757} \) (figure 6h), which suggests that the S \( \lambda 6757 \) feature is more reliable as S abundance indicator also for FGK dwarfs. It was once argued by Takeda (2007) based on the analysis of S \( \lambda 8693–5 \) lines that the dispersion of \([S/Fe] \) for 160 dwarfs is appreciably larger than that of \([Si/Fe] \) (cf. subsection 4.2 therein), in contrast to the result of Chen et al. (2002) who derived rather tight distributions for both \([S/Fe] \) and \([Si/Fe] \). However, given the present result, Takeda’s (2007) conclusion may be worth reconsideration, which may have been attributed to larger uncertainties in the S abundances derived therein.
4810.53 lines. Although the reason for this discrepancy is not clear, their results may have been influenced by blending effect and overestimated. On the other hand, the [Zn/H] values derived by Maldonado & Villaver (2016) as well as Maldonado, Villaver, & Eiroa (2013) are in agreement with our results, as illustrated in figure 7f and figure 7h. Maldonado et al. (2013) used Zn i 4810 and 6362 lines (as explicitly stated in Sect. 2.5 therein). Meanwhile, Maldonado and Villaver (2016) seem to have used only Zn i 6362 line, since they say that their line list was taken from Maldonado et al. (2015). The small changes between the results of their two papers may be mainly due to difference in the adopted Zn lines.

4.3. Trends of [S/Fe] and [Zn/Fe] for giants and dwarfs

Finally, we compare the metallicity-dependent trend of [S/Fe] (based on S i 6757 line) as well as [Zn/Fe] (based on Zn i 6362 line) derived for giants with that of dwarfs, and examine whether they satisfactorily match each other. This can be a valuable check for the validity of our S and Zn abundances of red giants as described in section 1.

The [X/Fe] vs. [Fe/H] diagrams (X is S or Zn) plotted for giants and dwarfs are shown in the left-side panels (a, b) of figure 8, where the mean ⟨[X/Fe]⟩ at each metallicity group (0.1 dex bin within −0.4 ≤ [Fe/H] ≤ +0.2) along with the distribution of ⟨[X/Fe]⟩giants − ⟨[X/Fe]⟩dwarfs are also presented in the corresponding right-side panels (c, d). We can confirm from this figure that [S/Fe]–[Fe/H] as well as [Zn/Fe]–[Fe/H] relations are essentially the same for both giants and dwarfs (the difference is only ≲ 0.05 dex), which substantiates the reliability of our S and Zn abundances derived for giants as well as dwarfs.

From the viewpoint of galactic chemical evolution, these similar runs of [S/Fe] and [Zn/Fe] with [Fe/H] (i.e., mild enhancement from ~0.0 to ~+0.3 as [Fe/H] is decreased from ~0 down to ~−1) are almost consistent with previous observational studies (e.g., Takada-Hidai et al. 2005 or Caffau et al. 2005 for S; Saito et al. 2009 for Zn) as well as theoretical predictions (e.g., Kobayashi et al. 2006; see also Kobayashi & Nomoto 2009 for Zn).

To conclude, the consequence of this study indicates that S and Zn abundances of evolved red giants (for which few credible results have been reported so far) can be reliably determined by carefully analyzing the S i 6757 and Zn i 6362 lines. Accordingly, we can employ (not only dwarfs but also) red giants to investigate the chemical evolution of S and Zn in the Galaxy by using these lines, though they are suitable only at the metallicity range of disk population (i.e. −1 ≲ [Fe/H]).

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5 Maldonado et al. (2015) state in their Sect. 2.6 that the Zn line was taken from Table 1 of Takeda and Honda (2005). But this must be incorrect, since any Zn line is not included therein. Instead, we consider that they adopted the Zn i 6362 line from Table 4 of Ramírez, Meléndez, and Asplund (2014) which was also referenced by them.
5. Summary and conclusion

Since sulfur and zinc belong to chemically volatile species, they play important roles in stellar spectroscopy because of being usable as depletion-free tracers for studying the galactic chemical evolution.

However, regarding stars of disk population, spectroscopic studies of S and Zn abundances have been mostly directed to unevolved dwarfs. As a matter of fact, despite that several extensive abundance studies of evolved red giants have been published in the past decade, reliable abundance determinations for these two elements seem to be rare.

Given this situation, we decided to establish the abundances of S and Zn for 239 apparently bright GK giants (in the metallicity range of $-0.8 \lesssim [\text{Fe/H}] \lesssim +0.2$) by applying the spectrum-fitting technique to S\,i 8694–5, S\,i 6757, and Zn 6362 lines, where the non-LTE effect was also taken into account. Besides, S and Zn abundances for 160 FGK dwarfs were also determined in the same manner, which are to used for comparison.

The non-LTE corrections for the S and Zn abundances derived from these lines turned out mostly $\lesssim 0.1$ dex (though amounting up to $\sim 0.2$–$0.3$ dex in some exceptional cases of S\,i 8695) and not very significant. The S\,i 6757 feature was found to be more reliable as an abundance indicator than S\,i 8694–5 for the case of red giants, because the latter appears to suffers appreciable blending with unidentified lines.

The finally obtained [S/Fe]–[Fe/H] and [Zn/Fe]–[Fe/H] relations for GK giants were confirmed to be in good agreement with those for FGK dwarfs, indicating that S and Zn abundances of red giants are reliably determinable from the S\,i 6757 and Zn 6362 lines.

Consequently, not only unevolved main-sequence stars but also evolved red giant stars can be exploited as probe to study the chemical evolution history of S and Zn in the regime of disk metallicity.

Data reduction was in part carried out by using the common-use data analysis computer system at the Astronomy Data Center (ADC) of the National Astronomical Observatory of Japan.
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### Table 1. Brief outline of observational data, atmospheric parameters, and line-strength measurements.

|                               | 239 GK giants | 160 FGK dwarfs |
|-------------------------------|---------------|----------------|
| **Basic observational data**  |               |                |
| Observation years             | 2012–2013     | 2000–2003      |
| Wavelength range              | 5100–8800 Å   | 5000–8800 Å    |
| (cf. Paper II)                | (cf. Takeda et al. 2005a) |
| Spectrum resolution           | ~ 67000       | ~ 67000        |
| **Atmospheric parameters**    |               |                |
| Method                        | Using FeI/FeII lines | Using FeI/FeII lines |
|                               | based on 2000–2005 data | based on the same 2000–2003 data |
|                               | (cf. Paper I) | (cf. Takeda et al. 2005b) |
| $T_{\text{eff}}$ (K)          | ~ 4500–5600   | ~ 5000–7000    |
| log g (cm s$^{-2}$/dex)       | ~ 1.4–3.5     | ~ 3.1–4.9      |
| $v_t$ (km s$^{-1}$)           | ~ 1.0–3.2     | ~ 0.5–3.0      |
| $\text{[Fe/H]}$ (dex)         | ~ −0.8 to ~ +0.2 | ~ −1.3 to ~ +0.5 |
| **Line-strength evaluation**  |               |                |
| $\text{Si}$ 8695             | fitting (figure 1 of this paper) | fitting (Fig. 4 of Takeda 2007) |
| $\text{Si}$ 6757             | fitting (figure 2 of this paper) | fitting (figure 3 of this paper) |
| $\text{Zn}$ 6362             | fitting (Fig. 4 of Paper II) | direct W measurement (cf. Takeda 2007) |

### Table 2. Atomic data of the relevant $\text{Si}$ and $\text{Zn}$ lines.

| Species | Line | RMT | Multiplet | $\lambda$ (Å) | $\chi_{\text{low}}$ (eV) | log gf | Gammar | Gammas | Gammaw |
|---------|------|-----|-----------|----------------|--------------------------|--------|--------|--------|--------|
| $\text{Si}$ | 8693 | 6   | 4p $^3P_3 - 4d ~^3D_2^o$ | 8693.137 | 7.870 | −1.370 | 7.62 | −4.41 | (−7.30) |
| $\text{Si}$ | 8694 | 6   | 4p $^3P_3 - 4d ~^3D_2^o$ | 8693.931 | 7.870 | −0.510 | 7.62 | −4.41 | (−7.30) |
| $\text{Si}$ | 8695 | 6   | 4p $^3P_3 - 4d ~^3D_4^o$ | 8694.626 | 7.870 | +0.080 | 7.62 | −4.41 | (−7.30) |
| $\text{Si}$ | 6757 | 8   | 4p $^3P_3 - 5d ~^3D_2^o$ | 6756.851 | 7.870 | −1.760 | 7.59 | −3.86 | (−7.13) |
|          | 8   | 4p $^3P_3 - 5d ~^3D_4^o$ | 6757.007 | 7.870 | −0.900 | 7.59 | −3.86 | (−7.13) |
|          | 8   | 4p $^3P_3 - 5d ~^3D_4^o$ | 6757.171 | 7.870 | −0.310 | 7.59 | −3.86 | (−7.13) |
| $\text{Zn}$ | 6362 | 6   | 4p $^1P_1^o - 4d ~^1D_2$ | 6362.338 | 5.796 | +0.150 | (7.74) | (−5.71) | (−7.45) |

All data were taken from Kurucz and Bell’s (1995) compilation as far as available. RMT is the multiplet number given in the Revised Multiplet Table (Moore 1959). Gammar is the radiation damping constant, log $\gamma_{\text{rad}}$. Gammas is the Stark damping width per electron density at $10^4$ K, log($\gamma_{e}/N_e$). Gammaw is the van der Waals damping width per hydrogen density at $10^4$ K, log($\gamma_{w}/N_H$). Note that the values in parentheses are the default damping parameters computed within the Kurucz’s WIDTH program (cf. Leusin, Topil’skaya 1987), because of being unavailable in Kurucz and Bell (1995). The meanings of other columns are self-explanatory.
Table 3. Abundance variations in response to changing atmospheric parameters.

| Line    | $\Delta T_u$ | $\Delta T_-^+$ | $\Delta g^+$ | $\Delta g^-_u$ | $\Delta v^+_u$ | $\Delta v^-_u$ |
|---------|--------------|----------------|--------------|----------------|----------------|----------------|
| Si 8695 | -0.016 (0.005) | +0.016 (0.006) | -0.123 (0.013) | +0.135 (0.015) | +0.090 (0.005) | -0.091 (0.004) |
| Si 6757 | -0.006 (0.001) | +0.007 (0.001) | -0.092 (0.010) | +0.103 (0.013) | +0.079 (0.003) | -0.079 (0.003) |
| Zn 6362 | -0.022 (0.005) | +0.025 (0.005) | -0.047 (0.019) | +0.060 (0.020) | +0.067 (0.009) | -0.065 (0.010) |

Note. Changes of the abundances (expressed in dex) derived from each line in response to varying $T_{\text{eff}}$ by $\pm 100$ K, $\log g$ by $\pm 0.2$ dex, and $v_t$ by $\pm 0.2$ km s$^{-1}$. Shown are the mean values averaged over each of the 239 stars, while those in parentheses are the standard deviations.
Fig. 1. Synthetic spectrum fitting for 239 GK giants in the 8691–8696 Å region comprising the S i 8693–5 lines. The best-fit theoretical spectra are shown by blue solid lines, and the observed data are plotted by red open circles (while those masked/disregarded in the fitting are highlighted in green). A vertical offset of 0.1 (in terms of the normalized flux with respect to the continuum) is applied to each spectrum relative to the adjacent ones. Each of the spectra are arranged in the increasing order of HD number (indicated on the left to each spectrum). The wavelength scale of each spectrum is adjusted to the laboratory system.
Fig. 2. Synthetic spectrum fitting for 239 GK giants in the 6756–6758.1 Å region comprising the S i 6757 line feature. A vertical offset of 0.05 is applied to each spectrum. Otherwise, the same as in figure 1.
Fig. 3. Synthetic spectrum fitting for 160 FGK dwarfs (and subgiants) in the 6756–6758.1 Å region comprising the S I 6757 line feature. Otherwise, the same as in figure 1.
Fig. 4. Equivalent widths ($W$) of S $\text{i}$ 8695, S $\text{i}$ 6757, and Zn $\text{i}$ 6362 lines are plotted against the atmospheric parameters in panels (a)–(f), while the dependences of non-LTE corrections ($\Delta$) upon $W$ are shown in panels (g)–(i): (a) $W_{8695}$ vs. $T_{\text{eff}}$, (b) $W_{6757}$ vs. $T_{\text{eff}}$, (c) $W_{6362}$ vs. $T_{\text{eff}}$, (d) $W_{8695}$ vs. log $g$, (e) $W_{6757}$ vs. log $g$, (f) $W_{6362}$ vs. log $g$, (g) $\Delta_{8695}^{\text{NLTE}}$ vs. $W_{8695}$, (h) $\Delta_{6757}^{\text{NLTE}}$ vs. $W_{6757}$, and (i) $\Delta_{6362}^{\text{NLTE}}$ vs. $W_{6362}$. The results for 239 GK giants are shown in blue filled symbols, while those for 160 FGK dwarfs are in open green symbols. In particular, the solar value is indicated by a large double circle in each panel.
Fig. 5. Non-LTE abundances ($A$) derived from S i 8695, S i 6757, and Zn i 6362 lines are plotted against the atmospheric parameters in panels (a)–(f), where the meanings of the symbols are the same as in figure 4: (a) $A$(S)$_{8695}$ vs. $T_{\text{eff}}$, (b) $A$(S)$_{6757}$ vs. $T_{\text{eff}}$, (c) $A$(Zn)$_{6362}$ vs. $T_{\text{eff}}$, (d) $A$(S)$_{8695}$ vs. $\log g$, (e) $A$(S)$_{6757}$ vs. $\log g$, and (f) $A$(Zn)$_{6362}$ vs. $\log g$. Panels (g) and (h) show the $A$(S)$_{6757}$ vs. $A$(S)$_{8695}$ correlations for GK giants and FGK dwarfs, respectively.
Fig. 6. [Fe/H]-dependences of equivalent widths (W), non-LTE corrections (∆), and [X/Fe] ratios (X is S or Zn), derived from S I 8695, S I 6757, and Zn I 6362 lines, where the meanings of the symbols are the same as in figure 4: (a) $W_{8695}$, (b) $W_{6757}$, (c) $W_{6362}$, (d) $\Delta_{8695}$, (e) $\Delta_{6757}$, (f) $\Delta_{6362}$, (g) [$S/Fe]_{8695}$, (h) [$S/Fe]_{6757}$, and (i) [$Zn/Fe]_{6362}$. In panels (g)–(h), the results for FGK dwarfs are shown with an offset of $-1$ dex relative to those of GK giants.
Fig. 7. Comparison of our finally adopted $[\text{S/}H]_{6757}$ or $[\text{Zn/}H]_{6362}$ results of GK giants with those of the common stars available in various literature: (a) $[\text{S/}H]$ from Luck (2015), (b) $[\text{Zn/}H]$ from Luck (2015), (c) $[\text{S/}H]$ from Luck & Wepfer (1995), (d) $[\text{Zn/}H]$ from Luck & Wepfer (1995), (e) $[\text{S/}H]$ from Maldonado & Villaver (2016), (f) $[\text{Zn/}H]$ from Maldonado & Villaver (2016), (f) $[\text{Zn/}H]$ from Jofré et al. (2015), and (g) $[\text{Zn/}H]$ from Maldonado et al. (2013). Filled circles ··· comparison of $[\text{S/}H]$, open circles ··· comparison of $[\text{Zn/}H]$. 
Fig. 8. Left-hand panels (a, b) show the comparison of \([\text{S/Fe}]\) (from \(\text{S} \, \text{i} \, 6757\)) vs. \([\text{Fe/H}]\) and \([\text{Zn/Fe}]\) (from \(\text{Zn} \, \text{i} \, 6362\)) vs. \([\text{Fe/H}]\) relations derived in this study for 239 G–K giants (filled symbols) with those of 160 FGK dwarfs (open symbols). Symbols in the right-side panels (c, d) give the mean \(\langle [\text{S/Fe}] \rangle\) and \(\langle [\text{Zn/Fe}] \rangle\) at each metallicity group (0.1 dex bin within \(-0.4 \leq [\text{Fe/H}] \leq +0.2\)) where error bars denote the standard deviations, while bar graphs represent the mean abundance differences between giants and dwarfs defined as \(\langle [\text{X/Fe}] \rangle_{\text{giants}} - \langle [\text{X/Fe}] \rangle_{\text{dwarfs}}\).