The Implementation of a Communication Deadlock Analysis Based on the Theory of Deadlock Analysis for the Actor Model

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Abstract

We present a unique approach for communication deadlock analysis for actor-model which has an under-approximated analysis result. Our analysis detects narrowly defined communication deadlocks by finding a cyclic dependency relation in a novel dependency graph called the *slave dependency graph*. The *slave dependency graph* is based on a new relationship between *Actors, slave dependency*, defined by us. After that, we implement this theory in Soot, an analysis tool for Java, and use it to analyze actor-based Java program realized by Akka, a Java library that allows actor-based programming. We argue that our analysis can detect a specific kind of communication deadlock with the precise result, but has many limitations.

Keywords

Actor Model, Communication Deadlock, Program Analysis, Akka, Soot, Dependency Graph

1. Introduction

Deadlock detection in concurrency programs is a well-studied topic. Although most of those studies focus on the traditional thread-based concurrency model, some studies still have significant influences on us so that we decided to bring their ideas into our own study. Flores-Montoya *et al.* [1] present an analysis that finds deadlocks in concurrency programs through dependency graph construction as the deadlock situation occurs when the dependency graph contains a circle. A. von Mayrhofer *et al.* [2] have also used the approach of Con-
trol-and-Communication Flow analysis to develop an algorithm that can detect communication deadlock in codes written in Ada, which is also a concurrency language. Their research, however, focuses on an algorithm that is capable of doing automated and efficient re-analysis after changes in the Ada code. J-L. Colaço et al. [3] present an analysis based on the type inference model for a primitive actor calculus to handle the situation of “orphan messages”, the messages received by actors while never being processed. This analysis is important in detecting communication deadlock, since orphan message is one of the causes of communication deadlock. Maria Christakis and Konstantinos Sagonas [4] propose a static analysis that could detect both Communication deadlock and Behavioral deadlock in the Erlang language. The analysis detects deadlocks by generating a control flow graph and finds whether the graph is a closed figure or not. If the graph is not closed, the whole program is considered to have a deadlock. This approach is by far one of the best approaches for detecting deadlocks, and it has demonstrated its feasibility by finding communication deadlocks in some open source libraries.

According to the definitions of behavioral deadlock and livelock, there is a wide variety of causes of these kinds of deadlocks; hence, it is hard for researchers to specify them and think of a general solution, resulting in little progress on analyzing these kinds of deadlocks. Therefore, the studies on communication deadlock are relatively more common, which make it easier for us to learn about and do some research on this topic. However, as we dive deep into the field of communication deadlock analysis for actor models, we find that there are a lot more theoretic studies than practical implementation of theories on finding communication deadlock. As a result, we develop a novel approach involving a “Slave Graph” (based on changes to an existing approach), for finding communication deadlock in an Actor System. After that, we implement our analysis theory and use an analysis tool, Soot, to look for communication deadlocks in a certain actor-based programming toolkit in Java, Akka, by checking the definition statements of specific actor classes inside the program being analyzed.

In this paper, we will be focusing on creating and testing a novel approach in finding communication deadlocks. The first part of this paper is about the introduction of the specific type of communication deadlock, “restricted communication deadlock” and the method of detecting it. In the rest of our paper, we put this method into actor-based-system tests, which we carefully projected, and evaluate it by discussing its advantages and disadvantages according to the test results.

2. Definition and Background Information

Actors are isolated concurrent entities that communicate through asynchronous messages and do not share state [5]. An actor responds to an incoming message by generating a finite set of communications sent to other actors, a new behavior
(which will govern the response to the next communication processed) and a finite set of new actors created [6]. The actor-based concurrency model is generally seen as an enhancement on the current thread-based concurrency model. Since actors can only interact with each other through the mean of message exchange, the states of each actor could only be subjected to mutation from itself, unlike how multiple thread can access the same process in the thread model. This means that the actor model is an effective solution to common problems in multi-thread program, such as data race conditions as well as deadlocks. However, thoughtless design of algorithms using the actor model is still possible to result in deadlocks [5].

Soot is a static program analysis framework developed by the Sable Research Group at McGill University. It processes Java code into a 3-address intermediate language called “Jimple”, which is suitable for static analysis. The modules in Soot support intraprocedural and interprocedural analysis, point-to analysis, def/use chain, and graph construction, but the users can also create their own analysis, like communication deadlock analysis in this research, based on the framework. Since Java by default does not support actor model concurrency, the programs we analyze in this research are Java codes written in Akka framework. Akka is an open-source toolkit developed by Lightbend that provide support for actor-model concurrency in both Java and Scala.

A communication deadlock is a condition in a system where two or more actors are blocked forever waiting for each other to do something. This condition is similar to traditional deadlocks known from thread-based programs [5]. However, we have a more specific situation of communication deadlock to analyze and have to narrow its definition. In our research, restricted communication deadlock occurs when two or more actors don’t send messages that are required by another actor and only declared by themselves, so that the actor system reaches a state that each actor in the actor system is waiting for another actor to send its message. An example of PingPong is given in Figure 1.

In Figure 1, Actor Ping and Pong both have the messages that are required by each other: Ping needs Pong_msg and Pong needs Ping_msg. However, neither of them will send those messages. Instead, they send “ok”. Hence, they reach a state of waiting for each other to send messages in line 2, which becomes a situation of restricted communication deadlock.

3. Development of Analysis Theory
3.1. Derivation from Dependency Graph

As we read through papers about finding communication deadlocks, we found a simple way to spot deadlocks, which is from the work of Flores-Montoya’s team. They created a kind of state dependency graph $G_c$ and state the definition of deadlock as following:

A program state $S$ is deadlock if and only if when its dependency graph $G_c$ contains a cycle [6].
However, we misunderstood the definition of “dependency graph $G_s$”, and went straight into the wrong direction of looking for cycles in data dependency and control dependency graphs. In fact, $G_s$ is actually built upon nodes like objects and task identifiers and whose edges are defined between objects and tasks, which is dramatically different from our work based on data dependency and control dependency graph.

At last, we found it couldn’t solve restricted communication deadlock and decided to take its idea of finding cycles in a kind of dependency graph and built our own dependency graph.

3.2. Slave Dependency Graph

3.2.1. Semantics

This section presents the semantics of actor-based language:

An Actor System $S$ is a set $S = \text{Actors}$ where Actors is the set of all created Actors.

An Actor is a term $\langle a, M, \text{RT} \{\text{msg}, t\} \rangle$ where $a$ is the Actor identifier, $M$ is the set of all messages created within the Actor, $\text{RT} \{\text{msg}, t\}$ is the set of all pairs of the message received and the message sent consequently, in which $\text{msg}$ means the message received by this Actor and $t$ means the message sent back by this Actor in response to the message it receives.

3.2.2. Definitions

Slave Dependency Relationship:

Given two Actors $A_1$ and $A_2$, we define their slave dependency relationship, $A_1$ is slave dependent on $A_2$ as follows:

$A_1 \langle a_1, MSG_{1}, \text{RT}_{1} \{\text{msg}, t_1\} \rangle$

$A_2 \langle a_2, MSG_{2}, \text{RT}_{2} \{\text{msg}, t_2\} \rangle$

$\exists x, \text{RT}_{1}[x] \cdot \text{msg} \in MSG_{2} \land \exists y, \text{RT}_{2}[y] \cdot \text{msg} \in MSG_{1} \land \forall z, \text{RT}_{2}[y] \cdot t_2 \neq \text{RT}_{1}[z] \cdot \text{msg}$

$A_1 \rightarrow A_2$

This type of relation corresponds to the situation when $A_1$ wants $A_2$ message and sends itself’s message to $A_2$ whereas $A_2$ receives the message from $A_1$ and doesn’t send back its message.

Specifically speaking, this definition of slave dependency relationship has three premises: $\exists x, \text{RT}_{1}[x] \cdot \text{msg} \in MSG_{2}$, $\exists y, \text{RT}_{2}[y] \cdot \text{msg} \in MSG_{1}$ and $\forall z, \text{RT}_{2}[y] \cdot t_2 \neq \text{RT}_{1}[z] \cdot \text{msg}$. I will explain each of them explicitly. The first premise is $\exists x, \text{RT}_{1}[x] \cdot \text{msg} \in MSG_{2}$, which means there exists a message possessed by $A_1$ and required by $A_2$. The second premise is $\exists y, \text{RT}_{2}[y] \cdot \text{msg} \in MSG_{1}$, simi-
lar to the previous one, which means there exists a message possessed by $A_2$ and required by $A_1$. The third premise is $\forall z. RT_1[y].t_z \neq RT_2[z].msg$, which means that when $A_2$ receives the required message from $A_1$, it doesn’t send back any message required by $A_1$. In this situation, the slave dependency that $A_1$ is “slave-dependent” on $A_2$ establishes.

**Slave Dependency Graph:**

Given an *Actor System* $S = \text{Actors}$, we define its *slave dependency graph* $G_s$ whose nodes are the existing *Actors* and whose edges are slave dependency relationship defined above.

**Restricted Communication deadlock:**

An *Actor System* $S$ has a restricted communication deadlock iff its *slave dependency graph* contains a cycle.

Singhal [7] defines that a resource deadlock is a set of processes in a state where each process in the set requests a resource held by another process in the set and a communication deadlock is in a similar situation whereas each process requires and waits for messages instead of resources. It is a situation alike in restricted communication deadlock in an *Actor System*, where each slave-dependent *Actor* awaits the message to be sent by the owner in a slave dependent relationship. Therefore, to achieve the state where every actor is restricted-communication-deadlocked, each of the *Actors* in the system needs to be slave dependent on anther, which consequently leads to a circle in *slave dependency graph*.

An example could be PingPong mentioned in the background information, in which PingPong can be expressed as follows:

$$
A_{Ping} \{Ping, \{Ping\_msg\}, \{\{Pong\_msg, \text{"ok"}\}\}\}
$$

$$
A_{Pong} \{Pong, \{Pong\_msg\}, \{\{Ping\_msg, \text{"ok"}\}\}\}
$$

Hence,

$$
Pong\_msg = Pong\_msg \land Ping\_msg = Ping\_msg \land \text{"ok"} \neq Pong\_msg
$$

$$
A_{Ping} \rightarrow A_{Pong}
$$

$$
Pong\_msg = Pong\_msg \land Pong\_msg = Pong\_msg \land \text{"ok"} \neq Pong\_msg
$$

$$
A_{Pong} \rightarrow A_{Ping}
$$

**3.3. Slave Chain**

After we generate a *slave dependency graph* for the actor model program, another algorithm will verify if the *slave dependency graph* has a cycle. Since the dependency graph is a collection of pairs of *Actors* in slave dependent relationship and we want to find a cycle in the graph, we merge these pairs into a chain called “Slave chain”. Here, we consider these pairs as a short chain of two *Actors*. We merge the *Slave Chain* with the next short chain iff the tail of the *Slave Chain* equals the head of the next one. After all the possible merges are finished, we look at the final product of *Slave Chain*. If the head of the *Slave Chain* equals its tail, which means the *Actors* in the chain are in a cyclic slave dependency re-
relationship, we consider that the *Actors* in this chain are in a restricted communication deadlock.

For example in *slave dependency graph* $G_S$:

$$A \rightarrow B \rightarrow C \rightarrow A$$

$G_S$ contains a restricted communication deadlock. As $B$ is the tail of the first pair as well as the head of the second pair, we merge them into a *Slave Chain*:

$$A \rightarrow B \rightarrow C \rightarrow A$$

We then merge the slave chain and the next pair for the same reason:

$$A \rightarrow B \rightarrow C \rightarrow A$$

Since the final *Slave Chain* $A \rightarrow B \rightarrow C \rightarrow A$ has its head and tail the same *Actor* $A$, and according to the theory above, the *Actors* in the chain, $A, B, C$, are in the state of restricted communication deadlock.

Continue, using the example of PingPong, as we have determined their slave dependency relationship:

$$\text{Ping Pong Pong Ping}$$

We find that the *Actor* at the tail of the first chain is also at the head of the second one. We then merge them together into

$$\text{Ping Pong Ping}$$

Since the head is also the tail in this chain, we conclude that the *Actors* $A_{Ping}$ and $A_{Pong}$ are in restricted communication deadlock.

4. Implementation of the Analysis Theory

4.1. Pseudocode of Analysis Program

Illustrated by **Algorithm 1**, internal `Transform()` is automatically executed by Soot, extracting statements within a class. In our implementation, we turn Soot to whole-program mode, so that Soot can extract statements from every class of Actors.

1) In line 1, we transform every line of code being analyzed into a statement by using Soot. We then store them in a list for further analysis.

2) In line 2, Statement Sequence is a set of consecutive statements in a program.

3) In line 3, we use the pattern we found from the source code of `.match()` function. As long as Statement Sequence match this pattern, we can determine *Actor*’s name and the receiving and sending of an actor, where the *Actor*’s name is after `@this`, the sending message is after `@parameter0` and receive message is after `new`.

```
Algorithm 1 Pseudocode of internalTransform()
1: <List> statements = soot.getStatement()
2: for StatementSequence ss in statements do
3:   if ss contains pattern <@this x1 ; @parameter0 x2 ; new x3> then
4:     Add Pair(x2, x3) to ReceSendMapping of ActorGraph x1
5:   end if
6:   if ss contains x1.lambda&createreserve< type x2 . . > then
7:     Add Pair(x2, null) to actor x1’s ReceSendMapping
8:   end if
9: end for
```
For example, the output of Soot shows the source code of `Actor Celcius`:

```java
[junit] r0 := @this: test1.Celsius
[junit] r1 := @parameter0: test1.AristotleAristotle_msg
[junit] $r3 = new test1.Celsius$Celsius_msg
```

4) In line 4, we add the receiving message and sending message pair to `RecvSendMapping`, which is a list of pairs describing how the `Actor` will react to the incoming message. `ActorGraph` is a data structure generally describing the characteristic of an `Actor`, which is a class contains `Actor's` name and `RecvSendMapping`.

5) In line 6, we also found a pattern to make sure we can find all of the receiving messages whether it sends the correct message or not. Here the predication means the `Actor` doesn’t send the right message.

6) In line 7, we do the similar thing in line 4, whereas we add null to its send message.

Illustrated by **Algorithm 2**, `findDependency()` is the method that search among `slave dependency graph` and reports restricted communication deadlocks. It is executed only once.

1) In line 1, we find all of the `Actors` by finding keyword `new` and `AbstractActor`, and store them into corresponding created `ActorGraph`. `graphList` is a list of all `ActorGraph` in the `Actor System`.

2) In line 2, we store `RecvSendMapping` in corresponding `ActorGraph`.

3) In lines 3-11, we check if the two `Actors` are in slave dependent relationship and add them to `slaveDependency` in a pair. `slaveDependency` is a list of pairs in which the key of the pair is the slave `Actor` and the value is the master `Actor`.

4) In line 13, we create a list `interval` to store the `Actors` being merged.

---

**Algorithm 2** Pseudocode of `findDependency()`

```pseudo
1: graphList = find all actors and create their ActorGraph
2: store RecvSendMapping in corresponding ActorGraph
3: for actor1, actor2 in graphList do
4:   if one of the actor1's recvMsgType matches actor2 then
5:     if one of the actor2's recvMsgType matches actor1 then
6:       if actor2 is not telling actor1 its recvMsg then
7:         Add Pair(actor1, actor2) to slaveDependency
8:       end if
9:     end if
10:   end if
11: end for
12: for Pair(p1, p2) in slaveDependency do
13:   interval = new List();
14:   if p1.getValue() equals p2.getKey() then
15:     Add p1.getValue() to interval
16:     Add Pair(Pair(p1.getKey(), p2.getValue()), interval) to slaveChains
17:   end if
18: end for
19: for Pair p in slaveChains do
20:   if p.getKey() is a pair with the same key and value then
21:     Report p
22: end if
23: end for
```
5) In line 15, we add the interval Actor to interval.
6) In line 16 we add the merged slave chain to slaveChains. slaveChains is a collection of pairs describing a series of Actors that are in slave dependency relationship.
7) In line 19-23, if we eventually get a Pair in slaveChains that has Pair(a,a), which means a circle in our slave dependency graph, the program will report an error by showing all the Actors in this chain are in the state of restricted communication deadlock.

4.2. Restrictions

For the above analysis to be employed in an actor model program, the program must satisfy two restrictions:

Restriction 1:
The message must be sent by the Actor that it is belonged to. Although in Akka, messages can technically be sent by Actors that does not own that particular message. However, since we couldn’t find the right code showing the receiving message is sent by which Actor, we have to restrict the message being sent. If a message can only be sent by one Actor, it is much easier for us to trace back where the message is from.

Restriction 2:
In each method match() of an Actor class, there is only one tell() function, whose caller of must be sender(). If there are multiple tell functions, no matter who the receiver is, we shall assume an Actor with two sender.tell(a). If the sender can reply to a, and the message it sent can also be replied by the first Actor, then it will do the two sender.tell(a) twice, because it received the same message twice. Thus, the Actor’s reply of the sender would increase exponentially with a base of two in this simplest base case. It would soon cause the entire program to go into a chaos either because of an infinite loop or recursion. It would be meaningless to write such codes in an Actor. Secondly, if we assume an Actor has a tell method with a caller “A”, where A can react to the kind of message the Actor sent—it still can’t imply that the message the Actor sent is strictly owned by itself. If we cannot identify it, we will not be sure whether the Actor A is dependent on the first Actor or the actual owner of the message or actually. Hence, it is also a meaningless piece of code.

4.3. Test Cases

Test Case 1:

| Ping | Pong |
|------|------|
| receive(Ping_msg, x → { sender().tell("ok") }); | receive(Pong_msg, x → { sender().tell("ok") }); |

Figure 2. Pseudocode of test case 1.
Figure 3. Slave dependency graph of test case 1.

Test Case 2:

| Aristotle | Beethoven | Celsius |
|-----------|-----------|---------|
| A.msg     | B.msg     | C.msg   |
| receive(B.msg, x -> {
  sender().tell("ok")
}) | receive(C.msg, x -> {
  sender().tell("ok")
}) | receive(D.msg, x -> {
  sender().tell(C.msg("ok"))
}) |
|          |          |         |
|          |          |         |
|          |          |         |

Figure 4. Pseudocode of test case 2.

Figure 5. Slave dependency graph of test case 2.

Test Case 3:

| Aristotle | Beethoven | Celsius |
|-----------|-----------|---------|
| A.msg     | B.msg     | C.msg   |
| receive(C.msg, x -> {
  sender().tell("ok")
}) | receive(A.msg, x -> {
  sender().tell("ok")
}) | receive(B.msg, x -> {
  sender().tell("ok")
}) |
|          |          |         |
|          |          |         |
|          |          |         |

Figure 6. Pseudocode of test case 3.
Test Case 4:

![Slave dependency graph of test case 3.](image)

**Figure 7.** Slave dependency graph of test case 3.

- Beethoven
  - B.msg
    - receive(A.msg, x →{
      - sender().tell("ok")
    })
  - E.msg
    - receive(D.msg, x →{
      - sender().tell("ok")
    })
- Celsius
  - C.msg
    - receive(D.msg, x →{
      - sender().tell("ok")
    })
  - F.msg
    - receive(E.msg, x →{
      - sender().tell("ok")
    })

![Pseudocode of test case 4.](image)

**Figure 8.** Pseudocode of test case 4.

![Slave dependency graph of test case 4.](image)

**Figure 9.** Slave dependency graph of test case 4.

Test Case 5:

![Pseudocode of test case 5.](image)

**Figure 10.** Pseudocode of test case 5.
The above Figure 2, Figure 4, Figure 6, Figure 8, Figure 10 illustrate the test cases which are used to test our implemented program, shown by Algorithm 1, Algorithm 2. Figure 3, Figure 5, Figure 7, Figure 9, Figure 11 depict the slave dependent relationship within the test cases for better understanding. We perform the analysis of the test cases each for 20 trails to test the stability of our test program’s performance and get the following table. From Table 1, we find that the accuracy of finding errors decreases as the number of Actors increases in the Actor System.

5. Related Work and Conclusions

Among all the related works, Flores-Montoya et al. [1] present an analysis that finds deadlocks in concurrency programs through dependency graph construction, and the deadlock situation occurs when the dependency graph contains a circle. Although our analysis also looks for deadlocks by finding a cyclic relation in a graph, we use a different graph, Slave Dependency Graph. On the other hand, the work of Flores Montoya et al. pays more attention to the thread-based concurrency programs. For A. von Mayrhauser et al. [2], their research, however, focuses on an algorithm that is capable of doing automated and efficient re-analysis after changes in the Ada code. Although this kind of algorithm is extremely useful in the setting of project maintenance, its focus on changes in the existing code and their impact is significantly different from our goal of detecting communication deadlock in the scope of the entire project. Although J-L. Colaço et al.’s work [3] directly relates to communication deadlock detection in actor model programs, their static detection algorithm in the paper could not detect all of the possible orphan messages, and the assist of dynamic detection still requires the locations of the remaining orphan messages. Maria Christakis and Konstantinos Sagonas’ work [4] is by far one of the best approaches for detecting deadlocks, and it has demonstrated its feasibility by finding communication deadlocks in some open source libraries. However, the approach we use is a more unique one.

We develop a novel dependency graph, slave dependency graph, in which we can find restricted communication deadlocks of an actor-based program, and demonstrate the algorithm’s feasibility by the implementation of building an analysis program. The analysis program can detect a specific kind of restricted communication deadlock in an actor-based Java program with Akka toolkit.
Table 1. Test results of 20 trails of the 5 test cases.

| Test Case | No Error Report | Partial Errors Report | All Errors Report |
|-----------|-----------------|-----------------------|-------------------|
| Test Case 1 | 0%              | 0%                    | 100%              |
| Test Case 2 | 10%             | 15%                   | 75%               |
| Test Case 3 | 10%             | 10%                   | 80%               |
| Test Case 4 | 15%             | 20%                   | 65%               |
| Test Case 5 | 5%              | 15%                   | 80%               |

There are two limitations in our research. The first one is about the imperfect precision of our analysis program. According to Table 1, we can see as the number of Actors in an Actor System increases, the percentage of failing report increases notably. This is due to the internalTransform() method provided by Soot, which extracts the key information of an Actor from the Java source code. It seems this method is run in multi-threaded for analyzing all actor classes, which may cause the pattern we found fails to construct ActorGraph with right information. Thus, the analysis program cannot report all the restricted communication deadlocks correctly from time to time. According to the test result, we believe the percentage of failing report would increase significantly, and we would have a smaller possibility to identify all the restricted communication deadlocks in a huge Actor System. Therefore, our analysis program is more suitable for small Actor System. The second limitation is due to our narrow definition of restricted communication deadlock. Since we have such a strict definition for restricted communication deadlock, the slave dependency relationship ignores situations. For example, an Actor receives a message and sends its message to another Actor. This restriction of definition makes our program only able to perform a limit under-approximation analysis of communication deadlock in an Actor System.

Authors Contribution

Among all the contribution of our work, Yupeng Xi initiated this research, designed the semantics and the theoretical approaches, analyze the test results, wrote most of the paper and coordinated the whole research process; Jianrui Zhang implement the theoretical approach by writing most of the deadlock-detecting program as well as the test cases; Furi Xiang gathered the information the paper required and did the whole analysis of existing related studies.

Conflicts of Interest

The authors declare no conflicts of interest regarding the publication of this paper.

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