The Subluminous Type Ia Supernova 1998de in NGC 252

MARYAM MODJAZ,1 WEIDONG LI,2 ALEXEI V. FILIPPENKO,2 JENNIFER Y. KING,1 DOUGLAS C. LEONARD,2 THOMAS MATHESON,3 AND RICHARD R. TREFERS2

Department of Astronomy, University of California, Berkeley, CA 94720-3411

AND

ADAM G. RIESS4

Space Telescope Science Institute, 3700 San Martin Drive, Baltimore, MD 21218

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ABSTRACT. We present spectroscopic and extensive photometric observations of supernova (SN) 1998de in the S0 galaxy NGC 252, discovered during the course of the Lick Observatory Supernova Search. These data, which span a time period of 8 days before to 76 days after $B$-band maximum, unambiguously establish SN 1998de as a peculiar and subluminous Type Ia supernova (SN Ia) with strong similarities to SN 1991bg, the prototype of these intrinsically dim SNe Ia. We find that SN 1998de, which has $m(B)_{p} - 1.95 \pm 0.09$ mag, rises and declines much faster than normal SNe Ia and does not exhibit the usual plateau in the $R$ band. In the $I$ band it shows a short plateau phase or possibly a secondary maximum, soon after the first maximum. We find that subluminous SNe Ia with the same value of $m(B)_{p}$ can have slightly different light curves at longer wavelengths. The notable spectroscopic similarities between SN 1998de and SN 1991bg are the wide Ti ii trough at 4100–4500 Å, the strong Ca ii features, and the early onset of the nebular phase. We observe that spectroscopic deviations of SN 1998de from SN 1991bg increase toward redder wavelengths. These deviations include the absence of the conspicuous Na i D absorption found in SN 1991bg at 5700 Å and the evolution of a region (6800–7600 Å) from featureless to feature-rich. Several lines of evidence suggest that SN 1998de was a slightly more powerful explosion than SN 1991bg. We discuss the implications of our observations for progenitor models and the explosion mechanism of peculiar, subluminous SNe Ia. The extensive photometric data make SN 1998de a better template than SN 1991bg for calibrating the low-luminosity end of the luminosity versus decline rate relationship.

1. INTRODUCTION

Supernovae (SNe) are classified into two main categories according to whether there are hydrogen lines present in their spectrum, usually taken near peak brightness: hydrogen-deficient supernovae are designated as Type I (SNe I), while those with hydrogen are Type II (SNe II). The category of SNe I is again subdivided into SNe Ia, Ib, or Ic, depending on whether they show further spectral features. Type Ia supernovae (SNe Ia) are identified by the appearance of a strong absorption feature at about 6150 Å due to blueshifted Si ii λ6355 (for reviews, see, e.g., Filippenko 1997; Harkness & Wheeler 1990).

A striking feature of SNe Ia has been their homogeneity; they have only moderate scatter in observed absolute peak magnitudes (Hamuy et al. 1996a) and similar light-curve shapes and spectra (e.g., Leibundgut & Pinto 1992; Branch & Tammann 1992; Filippenko 1997; Branch 1998). Moreover, the observed variations in luminosity among SNe Ia are found to be correlated with their light-curve shape, hence furnishing a tool to accurately calibrate the peak luminosity of SNe Ia [e.g., the $\Delta m_{15}(B)$ method: Phillips 1993; Hamuy et al. 1996a, 1996b; Phillips et al. 1999; the multicolor light-curve shape method: Riess, Press, & Kirshner 1996; Riess et al. 1998a; the stretch method: Perlmutter et al. 1997; the two-parameter method: Tripp 1998]. This has led to the successful usage of SNe Ia as “calibrated candles” for both nearby and cosmological distances and in the context of an array of applications such as tracing the expansion history of the universe (Riess et al. 1998a; Perlmutter et al. 1999), measuring the Hubble constant (e.g., Branch 1998; Suntzeff et al. 1999; Jha et al. 1999), studying the peculiar motions and bulk flows of galaxies (e.g., Riess, Press, & Kirshner 1995; Zehavi et al. 1998; Riess 2000), and probing the chemical evolution of galaxies (see, e.g., Pagel 1997 for a review).

In 1991, however, two nearby objects showed that there can
occasionally be extreme deviants among SNe Ia: SN 1991bg, an intrinsically very dim SN Ia (Filippenko et al. 1992b, hereafter F92; Leibundgut et al. 1993, hereafter L93; Ruiz-Lapuente et al. 1993; Turatto et al. 1996, hereafter T96; Mazzali et al. 1997, hereafter M97), and SN 1991T (Filippenko et al. 1992a; Ruiz-Lapuente et al. 1992; Phillips et al. 1992; Jeffery et al. 1992), an intrinsically overluminous object. Both of these SNe showed clear spectral differences from typical SNe Ia. Over the last decade, more instances have been found which exhibit distinct photometric and spectroscopic peculiarities, and it is now commonly thought that this group of so-called peculiar SNe Ia can be subdivided into SN 1991bg–like (subluminous) objects and SN 1991T–like (overluminous) objects. Although Branch, Fisher, & Nugent (1993) found that approximately 85% of all previously observed SNe Ia were normal (“Branch normal”), recent results by Li et al. (2000b, 2001a, 2001b) suggest an intrinsic peculiarity rate as high as 36% (20% SN 1991T–like, 16% SN 1991bg–like).

Whereas many normal SNe Ia have been studied in detail and well-sampled light curves have been published (e.g., Riess et al. 1999a), only a few peculiar SNe Ia (specifically of the subluminous variety) have been thoroughly observed. Examples include SN 1991bg, SN 1992K (Hamuy et al. 1994), and SN 1997cn (Turatto et al. 1998). A detailed study is necessary to address concerns about the utility of peculiar SNe Ia as reliable distance indicators, as well as to answer questions about their progenitor systems and explosion mechanisms.

In this paper we present SN 1998de as another instance of a peculiar, subluminous SN Ia. It was the eighth SN discovered by the Lick Observatory Supernova Search (LOSS; Treffers et al. 1997; Li et al. 2000a; A. Filippenko et al. 2001, in preparation) with the 0.75 m Katzman Automatic Imaging Telescope (KAIT; Richmond, Treffers, & Filippenko 1993; A. Filippenko et al. 2001, in preparation). A description of our observations and analysis, including methods of performing photometry, calibration of the measurements onto the standard Johnson-Cousins system, the resulting multicolor light curves, and comparisons between the light curves of SN 1998de, SN 1991bg, and other SNe Ia are given in § 2. The absolute magnitudes of SN 1998de are presented in § 3. Section 4 contains a description of the observations and analysis of the spectra of SN 1998de, including a thorough comparison of the spectra of SN 1998de, SN 1991bg, and the normal SN Ia 1994D. We discuss the implications of our observations on constraining progenitor models in § 5 and summarize our conclusions in § 6.

2. PHOTOMETRY

2.1. Observations and Reductions

SN 1998de, located 72″ from the nucleus of the S0 galaxy NGC 252, was discovered at $m \approx 18.4$ mag by Modjaz et al. (1998) in an unfiltered image obtained on 1998 July 23.5 and confirmed on July 24.5 during the LOSS. A KAIT image on July 19.5 already revealed a hint of the supernova, whereas a KAIT image on July 14.5 with a limiting magnitude of about 19 did not show any star at the supernova’s position, $\alpha = 0^h 48^m 06^s 88$ and $\delta = +27^\circ 37^\prime 28^\prime 5$ (equinox J2000.0). Because of the search’s small baseline (that is, the time interval to repeat observations of target galaxies: ~3–5 days), this supernova was caught 8 days prior to maximum brightness (on 1998 July 31.8 in $B$; see § 2.2). Garnavich, Jha, & Kirshner (1998) classified a spectrum of SN 1998de obtained on July 25.4 as Type Ia by the presence of a broad absorption feature of Si II at 6185 Å, noting that Ti II absorption at the blue end of the spectrum and strong Si II at 5800 Å suggested a peculiar and subluminous event, similar to SN 1991bg.

A KAIT monitoring program of broadband $BVRI$ photometry was established for SN 1998de 2 days after discovery, and it continued for about 2 months. Also, optical spectra of SN 1998de were obtained sporadically with the 3 m Shane reflector at Lick Observatory 1–2.5 months past maximum brightness. The photometric data were collected with the 512 × 512 pixel CCD camera (AP7) made by Apogee Instruments at the f/8.2 Cassegrain focus of KAIT with exposure times in the range of 300 s (in $R$ and $I$) and 600 s (in $B$ and $V$). The scale was 0.08 pixel$^{-1}$, and the field of view was 6.7′ × 6.7′. The typical seeing at Lick was around 3″ full width at half-maximum (FWHM). The bias and dark-current subtraction with subsequent twilight-sky flat-fielding were accomplished automatically at the telescope. Significant fringing in the $I$ band could not be completely removed, but this phenomenon has only a small impact on our results because the SN and comparison stars were considerably brighter than the background. This problem is presumably due to the fact that the infrared sky lines vary in brightness over time.

The telescope’s autoguiding device failed between July 25 and July 28. Multiple 60 s exposures were taken in each filter during that time, since the tracking mechanism was sufficiently accurate for exposure times of ≈100 s. They were later aligned and combined to form a single frame in each filter.

Figure 1 shows a KAIT $V$-band image taken on 1998 July 31 with SN 1998de and six comparison stars marked. Absolute calibration of the field was done on 1998 September 19, 20, and 21 by observing Landolt (1992) standard stars at different air masses throughout the photometric nights. Instrumental magnitudes for the standards were measured by employing simple aperture photometry with the IRAF$^7$ DAOPHOT package (Stetson 1987) and then used to determine transformation coefficients to the standard systems of Johnson (Johnson et al. 1966, for $BV$) and Cousins (Cousins 1981, for $RI$). The derived

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5 Note that the new Cepheid distance to NGC 4527, the host galaxy of SN 1991T, derived by Saha, Labhardt, & Posser (2000) suggests that SN 1991T is not as overluminous as previously claimed.

6 We use UT dates throughout this paper.

7 IRAF (Image Reduction and Analysis Facility) is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.
transformation coefficients and color terms were used to calibrate the sequence of six stars near SN 1998de that functioned as comparison stars for the supernova’s brightness. The magnitudes of these six local standard stars and the associated uncertainties derived by averaging over the three photometric nights are listed in Table 1. Since the field of view between July 25 and July 28 did not include the local standards E and F, they were not used when computing the brightness of SN 1998de for those dates.

We implemented the point-spread function (PSF) fitting technique for the differential photometry of the supernova relative to the comparison stars. Because of the fortunate position of the supernova far from the nucleus of the host galaxy in a region with a faint and smoothly varying background, measurement of the brightness of the supernova was not hampered by a complex environment, which usually necessitates template subtraction (e.g., Filippenko et al. 1986; Richmond et al. 1995). We could have chosen simple aperture photometry as our technique, but we decided against it; besides giving more accurate results than aperture photometry for objects projected upon slightly more complex regions (Schmidt et al. 1993), PSF fitting has the advantage of creating an image in which the measured objects can be subtracted. This can serve as an indicator of the quality of the brightness measurements of the comparison stars and the supernova.

Before the photometry procedure itself was initiated, special care was taken to remove cosmic rays, especially those around the PSF stars. Since our particular CCD camera is cooled.
thermoelectrically rather than with liquid nitrogen (for mechanical simplicity, and to decrease human maintenance of the robotic telescope), the temperature of the camera is not very stable and dark current is not always cleanly removed from the images. The resulting low-level dark-current residual varies during the night and has to be removed manually by adding or subtracting a few percent of the long-exposure dark-current image. The uncertainties introduced by the manual scaling of the dark current have only negligible effects on the brightness measurement of the high-contrast SN and the PSF stars.

The PSF for each image was determined with DAOPHOT, using well-isolated stars in the field, which are neither too bright (saturated) nor too faint. We used the inner core of SN 1998de and the local standards to fit the PSF in order to increase the signal-to-noise ratio (S/N). To measure the sky backgrounds of the SN and the local standards to fit the PSF in order to increase the signal-to-noise ratio (S/N). To measure the sky backgrounds of SN 1998de relative to the comparison stars.

The results of detailed examinations by Riess et al. (1999b) of the involved conversion parameters (e.g., the response function of KAIT’s CCD) yield a linear relation for stars between the standard color $B-V$ and the pseudocolor of the following form:

$$ V - C = C_{VC}(B - V). $$

Here $V$ is the standard Johnson passband $V$, and $C_{VC}$ is the slope of the linear relationship between the standard color $B-V$ and the pseudocolor $V-C$, empirically measured to be $0.33 \pm 0.10$ for the KAIT passbands (Riess et al. 1999b) with the imposed condition that $V-C = 0$ when $B-V = 0$.

Although the spectra of supernovae do not resemble those of normal stars (e.g., Filippenko 1997), their photometric behavior at very early times can be best approximated with a thermal model; their spectra are dominated by a thermal continuum (see Riess et al. 1999b for a detailed discussion). Thus, with the instrumental magnitudes for the unfiltered observations, the transformation equations for the supernova (SN) and the local standards (LS) are

$$ V_{SN} - c_{SN} = C_{VC}(B - V)_{SN} + A, $$

$$ V_{LS} - c_{LS} = C_{VC}(B - V)_{LS} + A. $$

Here the lowercase letter $c$ denotes the instrumental magnitudes in the pseudopassband “clear,” and $A$ denotes an air-mass extinction term that is the same for both SN and local standards in the same frame. Combining the two equations we can infer the standard $V$ magnitude of the supernova:

$$ V_{SN} = V_{LS} + (c_{SN} - c_{LS}) + C_{VC}(B - V)_{SN} - (B - V)_{LS}. $$

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**TABLE 1**

**Magnitudes of Local Standard Stars**

| Star | $B$ | $\sigma_B$ | $V$ | $\sigma_V$ | $R$ | $\sigma_R$ | $I$ | $\sigma_I$ |
|------|-----|------------|-----|-----------|-----|------------|-----|-----------|
| A    | 15.701 | 0.005     | 14.860 | 0.003     | 14.390 | 0.001     | 13.996 | 0.007     |
| B    | 14.462 | 0.009     | 13.708 | 0.003     | 13.268 | 0.003     | 12.916 | 0.003     |
| C    | 17.460 | 0.010     | 16.541 | 0.004     | 16.012 | 0.007     | 15.520 | 0.011     |
| D    | 13.736 | 0.005     | 13.092 | 0.003     | 12.733 | 0.003     | 12.443 | 0.003     |
| E    | 16.346 | 0.003     | 15.652 | 0.004     | 15.267 | 0.008     | 14.971 | 0.006     |
| F    | 16.486 | 0.006     | 15.727 | 0.003     | 15.315 | 0.010     | 14.988 | 0.011     |

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*Our Johnson $R$ filter, which gave rise to the rather large color term, has now been replaced by a Cousins/Bessell one, completing our new set of $UBVRI$ filters.*

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The amount of color evolution of the infant supernova, encapsulated by the term \((B-V)_{SN}\) for the discovery and confirmation observations, has a direct impact on our derived values for the standard magnitudes and cannot be directly measured but rather has to be derived from later points. We chose the value of \((B-V)_{SN}\) on the dates of the unfiltered observations (8 and 7 days before maximum brightness in the \(B\) passband) to be the same as on \(t = -5\) days, since the color of SN 1998de seems to evolve slowly at early times, as indicated by our data and in accordance with the behavior of most SNe Ia.

Despite the relative proximity of SN 1998de \((cz = 4950 \text{ km s}^{-1}; \text{see § 3})\), we applied \(K\)-corrections in order to account for the redshift effect. These are larger for SN 1998de than for normal SNe Ia, presumably due to its red color (see § 2.3; as Hamuy et al. 1993 show, there seems to be a tight relationship between color evolution and \(K\)-term curve). The \(K\)-corrections in \(B\), \(V\), and \(R\) were calculated using the spectra of SNe 1991bg and 1998de, but since most of the available spectra do not encompass the \(I\)-band wavelengths, the corrections in \(I\) are taken from normal SNe Ia.

Table 2 shows our final results for all photometric observations ranging from 8 days prior to \(B\) maximum until 51 days after maximum brightness. Uncertainties were estimated by combining in quadrature the errors given by the error analysis package in DAOPHOT with those introduced by the transformation of instrumental magnitudes onto the standard system and by the \(K\)-correction. Since SN 1998de was a relatively faint and red supernova, bad weather conditions influenced our data and affected the \(B\) images the most. For the sets of nights of August 11/12/13, August 16/17/18, and September 19/20/21, the \(B\) images had to be combined to yield one single image for each.
SUBLUMINOUS TYPE Ia SN 1998de IN NGC 252

set in order to obtain a sufficiently high S/N. The data for September 19/20/21, the last three nights of observation, were combined in this manner for all filters, since the SN was already very faint at that point. For the combined images, the epoch of the observation was taken to be August 12, August 17, and September 20, respectively.

2.2. Optical Light Curves

Figure 2 displays our $BVRI$ light curves of SN 1998de together with those of SN 1991bg (F92; L93). For all SN 1998de points except the marked ones, the uncertainties are smaller than the plotted symbols. The values for the date and the magnitude of the peak in each filter are given in Table 3; they were determined by fitting different spline functions and polynomials to the $BVRI$ light curves around maximum brightness. Since we have ample pre- and postmaximum data points, the uncertainties in our values are comparatively small, except in the $I$ band, where there does not seem to be one clear peak. Here, and in all subsequent discussions and figures, the variable $t$ denotes time since maximum brightness in the $B$ passband (JD = $2,451,026.3$).

In Figures 3 and 4, we compare the light curves of SN 1998de with those of several other well-observed SNe Ia representing the diversity of SN Ia light curves: SN 1991T (Ford et al. 1993 for $R$; Hamuy et al. 1996b for $BV$) as an example of an overluminous SN Ia, SN 1989B (Wells et al. 1994) and SN 1994D (Richmond et al. 1995) as examples of normal SNe Ia, and SN 1991bg (F92 for $RI$; L93 for $BV$) as the prototypical subluminous SN Ia. All light curves are shifted in time and peak magnitude to match those of SN 1998de with the time zero point being the date of maximum light in the $B$ passband. The data for the SN 1991bg–like objects SN 1992K (Hamuy et al. 1994) and SN 1997cn (Turatto et al. 1998) are not explicitly included here, since they are claimed to be twins to SN 1991bg both photometrically and spectroscopically, but comments and comparisons are provided.

Figures 2–4 show unambiguously that the early-time light curves of SN 1998de closely resemble those of SN 1991bg. Nevertheless, there seems to be a certain trend, where the discrepancies may increase with increasing wavelength of the passband so that the closest match between the two SNe is in the $B$ passband (except at late times). On the other hand, the most notable similarities in all filters are the narrow peak, beautifully exhibited by SN 1998de, and the rapid decline rate distinguishing these two SNe from the rest of the sample. Here SN 1998de displays among the best premaximum observations in our chosen sample—only SN 1994D was caught at a com-

Fig. 2.—The $B$, $V$, $R$, and $I$ light curves of SN 1998de, along with those of SN 1991bg ($RI$ from F92, “BAIT”; $BV$ from L93, “Leib”) which are shifted in time and peak magnitude to match those of SN 1998de. The time zero point is the date of maximum light in the $B$ passband, here 1998 July 31.8 UT.

Fig. 3.—The $B$ and $V$ light curves of SN 1998de, together with those of SN 1991bg (L93), SN 1991T (Hamuy et al. 1996b), SN 1989B (Wells et al. 1994), and SN 1994D (Richmond et al. 1995). All light curves are shifted in time and peak magnitude to match those of SN 1998de.

**TABLE 3**

| Filter | $B$ | $V$ | $R$ | $I$ |
|--------|-----|-----|-----|-----|
| Epoch of maximum | July 31.8 ± 0.1 | Aug 3.0 ± 0.2 | Aug 3.6 ± 0.5 | Aug 5.0 ± 1.1 |
| JD of maximum | 2,451,000.0 | 263 ± 1.0 | 285 ± 0.2 | 291 ± 0.5 | 30.5 ± 1.1 |
| Magnitude at maximum | 17.56 ± 0.04 | 16.82 ± 0.04 | 16.61 ± 0.04 | 16.71 ± 0.05 |
| $\Delta m_{15}$ | 1.95 ± 0.09 | 1.31 ± 0.06 | 1.08 ± 0.06 | 0.70 ± 0.09 |

2001 PASP, 113:308–325
parabolically early time. Unlike the case for SN 1991bg, for which there were no premaximum observations (or only a few in V; see L93), our data clearly establish SN 1998de as a fast riser.

The B-band light curve of SN 1998de (Fig. 3) matches that of SN 1991bg very closely at early times but seems to decline faster at late times (for \( t \approx \) 20 days). In accordance with Phillips (1993) and Hamuy et al. (1996a, 1996b), we define \( \Delta m_{15}(X) \) to be the decline (in magnitudes) during in the first 15 days after maximum brightness in the passband X, and we measure \( \Delta m_{15}(B) = 1.95 \pm 0.09 \) for SN 1998de. The uncertainty is the sum in quadrature of the uncertainty in the B-band peak magnitude, the change in the interpolated magnitude 15 days after peak (if the date of maximum is changed by the amount listed in Table 3), and the uncertainty of the observed magnitudes. This \( \Delta m_{15} \) value is nearly identical to that of SN 1991bg [\( \Delta m_{15}(B) = 1.93 \); Hamuy et al. 1996b; \( \Delta m_{15}(B) = 1.95 \); T96] and constitutes the largest value in our comparison sample of SNe Ia [\( \Delta m_{15}(B) = 1.31 \) for SN 1994D; Richmond et al. 1995; 0.94 for SN 1991T: Hamuy et al. 1996b; 1.31 for SN 1989B: Wells et al. 1994] and of all SNe Ia sampled during the Calán/Toledo Supernova Survey (Hamuy et al. 1996a).

There seems to be a steadily growing deviation from the SN 1991bg curve at late times (for \( t \approx \) 20 days), although the uncertainties of each individual measurement are relatively large. We can believe this deviation, since all data points of SN 1998de lie consistently below the SN 1991bg curve, and we conclude that it is due to an intrinsic difference between the photometric behavior of the two SNe at late times.

The V-band curve is shown in Figure 3 and reveals consistent similarities between SN 1998de and SN 1991bg, reinforcing the narrow-peak behavior. We measure \( \Delta m_{15}(V) = 1.31 \pm 0.06 \) (slightly smaller than the corresponding value for SN 1991bg, \( \Delta m_{15}(V) = 1.42 \) (L93)).

We present the R-band light curve in Figure 4 and note in SN 1998de the absence of the period of slower decline, the so-called plateau, which is characteristic of all normal SNe Ia at \( t \approx \) 20–30 days (Ford et al. 1993; Wells et al. 1994; Riess et al. 1999a). Rather, SN 1998de fades monotonically in R [with \( \Delta m_{15}(R) = 1.08 \pm 0.06 \)], a bit slower than SN 1991bg [\( \Delta m_{15}(R) = 1.18 \), based on our analysis of the F92 data]. There seems to be a region around the R-band maximum of SN 1998de that is not smooth, but with the present data set we cannot assess the reality of this. Perhaps significantly, the apparent “wiggle” appears to be even more pronounced in the I band (Fig. 4). Although these data points may say something about the supernova physics, we rather believe that they are two uncorrelated statistical deviations in the same direction.

After the initial peak in the I band 3–4 days past B maximum (Fig. 4), there is a plateau that extends out to \( t \approx \) 11 days. However, the I band does not show the kind of second maximum whose prominence is usually expected of normal SNe Ia, again very similar to the J-band behavior of SN 1991bg (though the plateau in SN 1998de is more pronounced than that of SN 1991bg). The two other well-studied SN 1991bg-like events, SN 1992K (Hamuy et al. 1994) and SN 1997cn (Turatto et al. 1998), were observed only well after maximum light, so there is no range of overlap. More comparisons with new SN 1991bg-like objects are needed to see whether one maximum, two maxima, or a maximum plus plateau are typically present in these kinds of SNe Ia.

It is interesting to note that if the I-band light curve is treated as having one broad peak, then its maximum in I is reached 8 or 9 days later in SN 1991bg-like SNe Ia when compared with normal SNe Ia, falling between the two maxima exhibited by the latter. The derived \( \Delta m_{15}(I) \) value is 0.70 \( \pm \) 0.09 for SN 1998de and 0.88 for SN 1991bg (based on our analysis of the F92 data).

We can also observe another trend, whose effect increases toward longer (redder) filter wavelength: although SN 1998de seems to concur completely with SN 1991bg in the B filter at early times, the deviations become stronger in the other filters, with the postmaximum light curves declining more slowly than those of SN 1991bg. This trend is embodied in the smaller \( \Delta m_{15} \) in all passbands (except B; see Table 3) when compared with those of SN 1991bg.

In summary, then, the light curves of SN 1998de closely resemble those of SN 1991bg and deviate notably from those of normal SNe Ia such as SN 1994D and overluminous ones such as SN 1991T. However, there are apparent differences between the light curves of SNe 1991bg and 1998de, especially at redder wavelengths, so we cannot simply regard SN 1998de as a mere twin of SN 1991bg. This conclusion, which is based on early- and intermediate-time photometry of SN 1998de, will be strengthened by the intermediate- and late-time spectral analysis in § 4.

### 2.3. Optical Color Curves

In Figure 5 we present the intrinsic optical color curves of SN 1998de, \( (B-V), (V-R), \) and \( (V-I) \), together with color...
curves of several other SNe Ia (1991bg, 1989B, 1994D, and 1991T) for comparison. For SN 1998de, a Galactic reddening [giving rise to a color excess of $E(B-V) = 0.06$ mag] was derived using full-sky maps of dust infrared emission (Schlegel, Finkbeiner, & Davis 1998). In order to calculate the color excess for the $I$ and $R$ passbands we adopt the standard reddening law parameterization, $E(V-I)/E(B-V) = 1.60$ and $E(V-R)/E(B-V) = 0.78$ (Savage & Mathis 1979). We follow Wells et al. (1994) in correcting the data for SN 1989B with $E(B-V) = 0.37$ mag, and we assume reddening $E(B-V)$ of 0.04 mag for SN 1994D (Richmond et al. 1995), 0.13 mag for SN 1991T (Phillips et al. 1992), and 0 mag for SN 1991bg (F92).

We assume that there is negligible reddening due to the dust in the host galaxy of SN 1998de for the following reasons. SN 1998de is located 72° from the nucleus of NGC 252, in the outskirts of a lenticular (S0) galaxy, where there is generally very little dust. Moreover, the spectra exhibit no conspicuous Na I D line at the redshift of the host galaxy. Unfortunately, we do not have enough $B-V$ points after $t = 32$ days in order to see whether the linear fit between intrinsic $B-V$ and time, which is described by Phillips et al. (1999) (and whose sample also includes SN 1991bg), is also valid for our case. Nevertheless, we note that the late-time color evolution of $(V-I)_0$ and $(V-R)_0$, for which we have two more data points, seems to conform with the color evolution of normal SNe Ia, thus possibly indicating that there is very little host galaxy extinction.

The prominent feature of the $(B-V)_0$ color evolution for both peculiar SNe (1991bg and 1998de) is their unusually red $(B-V)_0$ color at early epochs. At $B$ maximum SN 1998de has $(B-V)_0 = 0.56$ mag and SN 1991bg has $(B-V)_0 = 0.69$ mag, making SN 1998de about 0.6 mag redder than typical SNe Ia at this phase. Not only are the two peculiar SNe redder than normal SNe Ia, they also reach their reddest color (i.e., their maximum in a $B-V$ color curve) earlier than normal SNe Ia, at $t \approx 13$ days rather than at $t \approx 30$ days with $(B-V)_{max}^B = 1.45$ mag for SN 1991bg and $(B-V)_{max}^B = 1.62$ mag for SN 1998de. The $(V-R)_0$ color curve of SN 1998de shows a pattern of evolution which is again similar to that of SN 1991bg but seems to be overall bluer by $\sim 0.12$ mag. The region between $t = -5$ and $t = 4$ days, for which there are no SN 1991bg data, seems to reveal a fairly stable color of $(V-R)_0 \approx 0.15$ mag.

Thus, the $(V-I)_0$, $(V-R)_0$, and $(V-I)_0$ color curves of SN 1998de generally have a similar pattern of evolution and are strikingly redder than those of normal and overluminous SNe Ia at early times ($t \leq 40$ days). Each color curve has a maximum with the time differing only slightly: 13 days after $B$ maximum for the peak in $(B-V)_0$, and $t \approx 17$ days for $(V-R)_0$ and $(V-I)_0$.

### 3. Absolute Magnitudes

The light curves and color curves of SN 1998de suggest that it is subluminous, similar to SN 1991bg. In order to verify this, we need to find its absolute magnitude at maximum brightness and compare it with that of normal SNe Ia. Besides knowing the Galactic and extragalactic extinction, which was found in § 2.3, we need to accurately determine the distance to the host galaxy NGC 252 (UGC 491, PGC 2819).

NGC 252 is listed as the brightest member of group 12 of the Lyon Group of Galaxies Catalog (LGC; Garcia 1993) and also as a member of the Perseus supercluster (Vettolani & Baiesi Pilastrini 1987). Making use of the Lyon-Meudon Extragalactic Database (LEDA), we obtain a mean heliocentric estimate is close to those obtained by several other groups using different methods (e.g., neutral hydrogen line-width measurements by Eder, Giovanelli, & Haynes 1991; optical measurements by Huchra, Vogeley, & Geller 1999; see also de Vaucouleurs et al. 1991), all of which are between 4949 and 5023 km s$^{-1}$.

Since NGC 252 lies in the Hubble flow, we can use the

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10. As indicated by Kraan-Korteweg (1986), we can neglect the influence of the Virgo cluster on the host galaxy of SN 1998de.

2001 PASP, 113:308–325
survey and assuming in a linear perturbation theory.

SN 1998de is dimmer in the absolute Cepheid distance scale). Thus, its absolute magnitude is \( M \) mag at peak brightness in the \( B \) band at the time of explosion and \( H_0 \) km s\(^{-1}\) Mpc\(^{-1}\). For comparison, we also list the absolute magnitudes of the subluminous supernova and that it has magnitudes similar to those of SN 1991bg (on the surface brightness fluctuations [SBF] distance scale\(^{11}\)) in all four filters. These values are appreciably fainter and redder than the average,

\[
M_B = -18.64(\pm 0.05) + 5 \log \left( \frac{H_0}{65} \right) = -19.22 \text{ mag},
\]

\[
M_V = -18.59(\pm 0.06) + 5 \log \left( \frac{H_0}{65} \right) = -19.21 \text{ mag}
\]

for \( H_0 = 65 \) km s\(^{-1}\) Mpc\(^{-1}\) as found by Vaughan et al. (1995) for their ridge-line SNe Ia (i.e., SNe Ia that suffered little extinction, but were also not exceptionally luminous). SN 1998de is even more extreme when compared to the Riess et al. (1996) absolute magnitude template values \( M_B = -19.38 \) and \( M_V = -19.36 \) mag and the mean SN Ia magnitudes derived with the Cepheid distance calibration \( M_B = -19.65 \pm 0.13 \) and \( M_V = -19.60 \pm 0.11 \) mag; see Saha et al. (1995).

The high quality of the data combined with our accurate distance measurement (excluding uncertainties in \( H_0 \)) make SN 1998de an ideal candidate for testing current studies of the behavior of SNe Ia in the subluminous range. Riess et al. (1999b) determine the rise time (i.e., the time between explosion and

\[
\mu = (m - M) = 34.26(\pm 0.20) - 5 \log \left( \frac{H_0}{65} \right) \text{ mag}, \tag{9}
\]

where the uncertainties reflect a possible peculiar motion of \( \sigma = 420 \) km s\(^{-1}\) of the host galaxy with respect to the Hubble flow (M. Davis 2000, private communication\(^{11}\)).

Using apparent peak magnitudes as listed in Table 3, together with our estimates of the extinction and distance, we derive the peak absolute magnitudes for SN 1998de in all filters (Table 4). The quoted uncertainties are the sums in quadrature of the uncertainties in peak magnitude, extinction, and distance. For comparison, we also list the absolute magnitudes of the subluminous SN 1991bg, as well as the normal SN Ia 1994D.

Riess et al. (1996, 1998a) describe an empirical method (the multicolor light-curve shape; MLCS) to derive the absolute magnitude, distance, and total line-of-sight extinction of a Type Ia supernova. Applying the linear MLCS method to both light curves and color curves of SN 1998de, we derive a value of the “luminosity correction” \( \Delta = 1.42 \pm 0.15 \) mag and \( A_V = 0 \) mag. Given the uncertainties, this is indistinguishable from \( \Delta = 1.44 \pm 0.10 \) mag for SN 1991bg (Riess et al. 1996). The luminosity correction signifies the amount by which SN 1998de is dimmer in the \( V \) band at the time of \( B \)-band maximum than a normal SN Ia with \( \langle M_V \rangle = -19.36 \) mag (on the absolute Cepheid distance scale). Thus, its absolute magnitude is \( M_V = -17.96 \pm 0.15 \) mag at peak brightness in \( V \). This value is 0.33 mag brighter than our more direct estimate, 0.06 mag of Galactic reddening. The MLCS method attempts to match the light curve of SN 1998de with that of the template, which is generated using a “training set” of SNe Ia. But since this training set consists primarily of normal SNe Ia and includes only one confirmed subluminous supernova (SN 1991bg) and a proposed one (SN 1986G; see, e.g., F92), MLCS might be less reliable at low luminosities. Thus, we hesitate to adopt the luminosity of SN 1998de derived by Riess.\(^{12}\)

We can clearly discern from Table 4 that SN 1998de is a subluminous supernova and that it has magnitudes similar to those of SN 1991bg (on the surface brightness fluctuations [SBF] distance scale\(^{13}\)) in all four filters. These values are appreciably fainter and redder than the average,

\[
M_B = -18.64(\pm 0.05) + 5 \log \left( \frac{H_0}{65} \right) = -19.22 \text{ mag}, \tag{11}
\]

\[
M_V = -18.59(\pm 0.06) + 5 \log \left( \frac{H_0}{65} \right) = -19.21 \text{ mag}
\]

(Table 4), but considering the uncertainties in both methods, this is not a very significant discrepancy. MLCS also suggests that there is no extinction, while we assumed \( E(B - V) = 0.06 \) mag of Galactic reddening. The MLCS method attempts to match the light curve of SN 1998de with that of the template, which is generated using a “training set” of SNe Ia. But since this training set consists primarily of normal SNe Ia and includes only one confirmed subluminous supernova (SN 1991bg) and a proposed one (SN 1986G; see, e.g., F92), MLCS might be less reliable at low luminosities. Thus, we hesitate to adopt the luminosity of SN 1998de derived by Riess.\(^{12}\)

\(^{12}\) The “two-parameter luminosity correction” advocated by Tripp (1998) yields a corrected \( M_B = -18.84 \) mag for SN 1998de, significantly different from the value for normal SNe Ia (\( M_B = -19.36 \) mag; Riess et al. 1996). But this method is poorly calibrated for very red SNe Ia, and it does not distinguish between reddening by dust and intrinsically red colors. Thus, we do not adopt it here.

\(^{13}\) Note that the SBF method yields a Hubble constant of \( 67 \) km s\(^{-1}\) Mpc\(^{-1}\) (e.g., Tonry et al. 2000).

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\(^{11}\) The peculiar velocity was derived using predictions from the 1.2 Jy IRAS survey and assuming \( \beta = 0.5 \) in a linear perturbation theory.
corrected for Galactic reddening versus $\Delta m_{15}(B)$ (Fig. 6, open circles) and add our data points for SN 1998de (filled circles). Whereas SN 1992K seems to concur with the almost linear correlation (in fact, Phillips et al. 1999 find it to be quadratic), SN 1998de deviates from its expected behavior. However, more studies of subluminous SNe Ia are needed to accurately calibrate the luminosity versus decline rate relation at the subluminous end.

### 4. SPECTROSCOPY

#### 4.1. Observations and Reductions

Spectroscopic observations were conducted with the Lick 3 m Shane telescope using the Kast CCD spectrograph (Miller & Stone 1993) on the three dates listed in Table 5. The air mass was in all cases close to 1.0, and a slit width of 2″ was used.

All optical spectra were reduced and calibrated employing standard techniques. To remove near-infrared fringing in the CCD, flat-field exposures were taken at the position of the supernova, as were He-Hg-Cd-Ne-Ar lamp exposures for wavelength calibration. The spectra were corrected for the continuum atmospheric extinction using mean extinction curves, and their telluric lines were removed following a procedure similar to that of Wade & Horne (1988) and Bessell (1999). The final flux calibrations were derived from observations of one or more spectrophotometric standard stars (Oke & Gunn 1983). All spectra shown in this paper have been corrected for reddening (as in § 2.3) and for their redshift.

The spectral evolution of SN 1998de is illustrated in Figure 7. There was poor signal below 4000 Å and considerable fringing above 8000 Å, affecting our observations more at late times, where the fringe amplitude was much closer to the supernova brightness. The sharp and narrow “absorption lines” in the $t = 76$ day spectrum are noise spikes and cosmic rays, but we refrained from averaging or smoothing them in order to give an authentic impression of the quality of the data.

As mentioned in § 2.1, the spectrum reported by Garnavich et al. (1998) and taken $\approx 6$ days before $B$ maximum already shows the Ti ii absorption feature and a very strong Si ii feature at 5800 Å, suggesting SN 1998de to be an SN 1991bg–type Ia event. Unfortunately, we have no spectra of our own around maximum light, with which we could have checked the spectral...
sequencing method described by Nugent et al. (1995), who find a correlation between the strength of certain spectral features of SNe Ia and their absolute B magnitude. Our first spectrum was obtained 31 days after B maximum and resembles that of the peculiar SN Ia 1991bg. It exhibits the broad trough at 4100–4500 Å identified as Ti II (F92; T96; M97) and shows signs of an early onset of the nebular phase. On the other hand, apparent evidence for abundance or excitation anomalies is present when compared with SN 1991bg.

In the following, we adopt the line identifications for SNe Ia of Jeffery et al. (1992), of Kirshner et al. (1993), and also those of F92, L93, T96, and M97 for SN 1991bg–type events. Since the L93 absorption identifications refer only to the phase of B maximum and are not necessarily applicable at later epochs, we employ them with caution. We note that our line identifications for SN 1998de are not definitive since we have not conducted spectral synthesis calculations. The identification of emission lines, especially, on the basis of wavelength coincidences might be a precarious undertaking; because of the presence of a complex blend of P Cygni profiles on an underlying spectrum that varies rapidly with wavelength, the wavelengths of the emission peaks may be affected. We adopt the convention that wavelengths given in Å are measured wavelengths in the rest frame of the galaxy, whereas those preceded by a λ are laboratory wavelengths.

To illustrate the similarities and differences among SN 1998de, its close relative SN 1991bg, and the normal SN Ia 1994D, we plot the three epochs separately in Figures 8, 9, and 10. Although SN 1998de shares several of SN 1991bg’s unusual features in the wavelength range corresponding to the B band, it also exhibits notable disparities in the wavelength ranges of the V, R, and I bands. This is consistent with the trend seen in the light curves of SN 1998de, where the deviation from SN 1991bg increases with increasing band wavelengths. Thus, a good match in one passband (here the B band, perhaps the most frequently observed one) does not necessarily guarantee the same degree of similarity in the other passbands. This has ramifications for further studies of peculiar SNe Ia, calling for a broad passband coverage in both photometric and spectroscopic observations.

4.2. The Spectrum at 31 Days after B Maximum

In the t = 31 day spectrum (Fig. 8), Ca H & K is seen in both absorption and emission as a classical P Cygni profile, as expected for SNe Ia. However, whereas the emission component (at 3990 Å) stays the same, the absorption part (at 3790 Å) deepens as the object ages (Fig. 7, although it is hard to discern its exact strength because of noise and the absence of any other emission features at shorter wavelengths), similar to the trend observed with SN 1991bg, where it grew even deeper. The broad absorption trough between 4120 and 4460 Å, one of the most conspicuous and intriguing peculiarities of all very subluminous SNe Ia, such as SN 1991bg, has been identified with Fe II by L93 by matching wavelengths, while F92, Ruiz-Lapuente et al. (1993), and M97 attribute it to a blend of Ti II lines using spectral synthesis analysis. F92 and M97 suggest that Mg II λ4481 might also contribute to the absorption. Since the evidence for Ti II through the technique of spectral synthesis is more compelling, we adopt this particular interpretation. This trough contrasts sharply with the expected blend of Si, Mg, and Fe lines observed at comparable epochs in typical SNe Ia (e.g., Kirshner et al. 1993). Note that the trough in SN 1998de might be somewhat broader (by ~100 Å) than the one in the SN 1991bg spectrum.

The wavelength range between 3800 and 5540 Å provides an impressive match to that of SN 1991bg. The emission line at about 5540 Å has been attributed to [O I] λ5577 for SN 1991bg by F92 (see L93 for an alternative identification), indicating the early start of the nebular phase. If we apply this identification also to SN 1998de, a significant fraction of the unburned oxygen is visible in dense states outside the bulk of the ejecta, as suggested by M97 for SN 1991bg. L93 reject this interpretation, since the strength of the line and the absence of the [O I] doublet at 6300 Å would imply very high densities (n ≈ 10¹¹ oxygen atoms cm⁻³) and low temperatures (T_e < 2000 K) for reasonable electron density (n_e/n_oi = 1) and ionization (n_oi/n_oi = 10⁻³; L93). However, M97 present compelling and intriguing evidence with the use of Monte Carlo simulations that SN 1991bg shows an indication of a high oxygen abundance due to incomplete burning and low temperatures. Their calculations may also explain the unusual strength of the Ti II lines and the red color of SN 1991bg.

Broad emission features, which are stronger in both
SN 1991bg and SN 1998de than in SN 1994D and which are commonly observed in normal SNe Ia at later epochs (t ≥ 40 days) are the emission components of the Ca H & K feature and of the Ca II near-infrared triplet at 8700 Å, implying an early onset of the nebular phase.

One of the most unusual characteristics displayed by the intermediate and late-time spectra of SN 1991bg is a very strong and relatively narrow absorption line measured near 5700 Å, which increases in strength over time. As T96 show, this line, which is almost invisible in the maximum-light spectrum, persists for over 5 months with the line profile remaining nearly constant in time (FWHM ≈ 2500 km s⁻¹). If we identify it with Na I D (F92; see Fig. 7 of M97 for the reproduced Na I D line in a modeled spectrum), which indeed forms a broad absorption line in normal SNe Ia at this epoch, we obtain an expansion velocity of v_{Na I D} = 9400 km s⁻¹ for the absorbing layers. This is larger than the corresponding expansion velocity derived on the basis of the Si II λ6355 shift for the same epoch (v_{Si II} = 7000 km s⁻¹). Both the narrow width and the high expansion velocity indicate that the element responsible for the 5700 Å feature is situated in a relatively thin outer layer (since the velocity of a shell is proportional to its radius at this phase). This could be evidence for abundance stratification in the ejecta of SN 1991bg as pointed out by T96. An alternative interpretation is given by L93, who propose that the 5700 Å feature is due to a blend of Si II lines, but since it is very narrow, we hesitate to adopt this identification (although Si II might be present, but contaminated by the very strong Na I D).

Remarkably, the 5700 Å feature is not visible in any of the SN 1998de spectra, whereas other SN 1991bg-type objects such as SN 1997cn (Turatto et al. 1998) and SN 1992K (Hamuy et al. 1994) display it. SN 1998de thus adds to the “mystery” of this conspicuous feature. It is interesting that the first major mismatch between SN 1998de and SN 1991bg occurs in the passband corresponding to the V band. It is tempting to correlate the photometric mismatch found in the V filter for t = 31 days (SN 1998de being ~0.2 mag dimmer than SN 1991bg) with the 5700 Å feature and other, minor lines.

In SN 1998de, as in SN 1991bg, the primary characteristic feature of SNe Ia, Si II λ6355, seems to be contaminated by another absorption line. Unlike the case in SN 1991bg, however, both wings appear to be broadened owing to the presence of other elements. Instead of a narrow and well-defined core as found in normal SNe Ia such as SN 1994D, we see a V-shaped feature that fades as the supernova ages. Garnavich...
et al. (1998) measure at $t = -6$ days the minimum of Si II λ6355 at 6185 Å and thus infer a photospheric expansion velocity of 13,300 km s$^{-1}$ for SN 1998de, after correcting for the host galaxy’s redshift. This is consistent with expansion velocities for normal SNe Ia which range between 11,000 and 13,000 km s$^{-1}$ at maximum brightness (Branch, Drucker, & Jeffery 1988; Barbon et al. 1990) and possibly with SN 1991bg, which showed a velocity of 9900 km s$^{-1}$ at maximum light (F92). Applying the same technique, we find an expansion velocity of 7080 km s$^{-1}$ for $t = 31$ days, which is in excellent agreement with a velocity of ~7000 km s$^{-1}$ for SN 1991bg at $t = 27$ days and considerably smaller than the photospheric expansion velocity of SN 1994D (v = 8970 km s$^{-1}$) at the same epoch. These results are very interesting: whereas SN 1991bg showed a lower expansion velocity than normal SNe Ia, which led to the theoretical insights that the mass of the ejecta might be small for consistency with an early onset of the nebular phase and that complete burning was confined to the innermost regions (T96; M97), SN 1998de might not show such a clear trend. Again, early-time spectra would have been more useful for monitoring the development of the expansion velocity.

Note the broad emission near 6520 Å, which usually begins to develop around $t = 2$ weeks for normal SNe Ia and which is clearly visible at $t \approx 4$ weeks in the spectra of SNe 1994D, 1991bg, and SN 1998de. It remains present thereafter with some changes in shape and can be identified with Fe II and later [Fe II] (L93; Filippenko 1997), and not with H$_\alpha$ as one might erroneously infer.

A peculiarity which distinguishes SN 1998de from both SN 1991bg–like objects and normal SNe Ia is the nearly featureless region from 6800 to 7600 Å which lies in a wavelength range corresponding to the $I$ passband. The prominent absorption component of the O I λ7774 P Cygni feature and its contamination by Mg II λλ7877–7896 in the red wing as seen in SN 1991bg (F92; M97; T96) and its twins (SNe 1997cn, 1992K) is not present, whereas the hump near 7760 Å is probably due to the emission component of O I λ7774 (but at a slightly longer wavelength when compared to SN 1991bg: F92; L93; M97). The spectrum of SN 1998de may show a small indentation at the expected position of Mg II, but the quality of the data is too poor for a definite conclusion. M97 claim that the observed behavior of the O I λ7774 absorption.

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14 Since the Si II λ6355 line is not visible in later spectra, we cannot use it to obtain the expansion velocity, but by then the nebular phase has completely emerged and the photospheric model is no longer applicable.
in SN 1991bg, which does not evolve redward (i.e., to lower velocities) during the first 2 weeks after \( V \) maximum, is indicative of an outer oxygen shell containing unburned material from the progenitor, for which the observed \([\text{O} \, \text{i}] \lambda 5577\) emission was the first clue. The absence of the \([\text{O} \, \text{i}] \lambda 7774\) absorption line in SN 1998de could be due to possible contamination by a blend of broad emission lines, but no likely candidates are known. A more feasible explanation could be that there is not as much \([\text{O} \, \text{i}]\) present in SN 1998de as in SN 1991bg. If so, perhaps SN 1998de does not have as much unburned oxygen left as did SN 1991bg.

As in other SN Ia spectra, the obvious P Cygni profile of the \( \text{Ca} \, \text{ii} \) near-infrared triplet is visible between 8000 and 8700 Å, although both absorption and emission are much stronger than usual, similar to the appearance of SN 1991bg. Early-time spectra would be more conclusive for displaying the effects of color evolution—indeed, we would expect those spectra to be redder than in normal SNe Ia. The consistently red color of SN 1991bg was interpreted by M97 as an indication for a lower photospheric temperature, as would be expected with the presence of only incomplete nuclear burning.

4.3. The Spectra at 51 and 76 Days after \( B \) Maximum

Figure 9 displays the spectra of SNe 1998de, 1991bg, and 1994D at about the same epoch of \( t \approx 7 \) weeks, while Figure 10 shows the spectra of the same SNe at \( t \approx 12 \) weeks. Our initial conclusion—that differences between SN 1998de and SN 1991bg increase with increasing wavelength—is confirmed. Besides the further emergence of emission lines, the following major changes have occurred in SN 1998de and are clearly visible in Figure 10: (1) the \([\text{O} \, \text{i}] \lambda 5577\) and the \([\text{O} \, \text{i}] \lambda 7774\) emission features have weakened and become broader; (2) pronounced emission has appeared at 5900 Å whose position coincides with the \([\text{Co} \, \text{iii}]\) emission in SN 1991bg (L93; T96; M97); (3) a deep and broad absorption trough is present at \( \sim 6800 \) Å adjacent to an emerging broad emission feature at \( \sim 7200 \) Å; and (4) \([\text{Si} \, \text{ii}] \lambda 6355\) has disappeared whereas \([\text{Si} \, \text{ii}] \lambda 5968\) seems to have gained strength and may be contaminated in its blue wing.

Most of the emission lines at this nebular stage are identified with forbidden lines of Fe and Co, the decay products of \(^{56}\text{Ni}\), while the \( \text{Ca} \, \text{ii} \) emission is still strong in the spectra of both SN 1998de and SN 1991bg (Fig. 10). The oxygen line deterioration can be explained by the fact that the photosphere is receding into the central parts of the ejecta, where the higher mass elements have been produced. The drifting of emission lines to the red, most notably the \([\text{Fe} \, \text{iii}]\) feature at 4615 Å, illustrates the decrease in the expansion velocity as we look deeper into the ejecta. The broad absorption at 6800 Å is most
probably due to Fe II, whose signature is visible in SN 1991bg as well as in SN 1994D (and generally in SNe Ia). The adjacent emission at 7200 Å, which is only visible at τ = 76 days, could be tentatively identified as a blend of [Ca II] λλ7291, 7324 (F92; Ruiz-Lapuente et al. 1993) or a blend of [Fe II] (L93). Note that the corresponding feature in SN 1991bg is observed at a slightly longer wavelength (7250 Å) and that it dominates the spectrum of SN 1991bg, whereas it is very broad and not as distinct in the spectrum of SN 1998de (also the red shoulder seems to be contaminated) and is absent in the case of SN 1994D.

Since the Si II λ5968 absorption is not contaminated by a Na I D line, it is easily visible as a distinct feature at nearly the same position as in the τ = 31 day spectrum, only deeper. Because this Si II feature deepens between the two last epochs and is accompanied by a receding photosphere which reveals the deeper layers, we could have evidence that nuclear burning was incomplete in these layers.

The dominant and narrow [Co III] emission feature of SN 1991bg visible at 5908 Å has been regarded by M97 as an indication of a centrally peaked distribution of 56Ni and as the result of complete incineration of matter in the central part of the ejecta, assuming that the emissivity is proportional to the Co abundance and to the local gamma-ray deposition rate in the Co-rich material. Combining this with their observation of oxygen during the photospheric phase, M97 suggest that complete burning did not take place everywhere and that the outer layers underwent incomplete burning, in contrast to the inner part. For SN 1998de, the corresponding [Co III] emission is observed at nearly the same position of around 5900 Å in both the τ = 51 and τ = 76 day spectra; however, it is not as narrow as in SN 1991bg. This might indicate that complete incineration extended to a larger radius in SN 1998de than it did in the case of SN 1991bg. [Co III] λλ6129, 6197 emission is also found at around 6210 Å in the τ = 76 day spectrum, matching the features at 6144 and 6204 Å in SN 1991bg (T96). Furthermore, we see the aforementioned emission of [Fe II] (L93; see T96 for alternative identification) at around 6520 Å in the spectrum of SN 1998de, a feature which is found in all three SNe (1994D, 1991bg, 1998de) and which was already visible in their intermediate-phase spectra (see Fig. 8).

The Ti II trough between 4100 and 4500 Å, a primary characteristic of SN 1991bg–type objects, is still distinctly visible at these late times. Thus, this feature can be used as a powerful tool for distinguishing between peculiar and normal SNe Ia at all epochs, even for SNe at large redshifts (whose rest-frame visible and red spectral regions are shifted in the range where the infrared fringing of CCDs affects the data). The strong presence of Ti II can be explained either in terms of abundance anomalies or by excitation differences. Both F92 and M97 favor the interpretation that the red color and hence low excitation temperature is largely responsible for producing the observed strong Ti II lines in local thermodynamic equilibrium (see, e.g., Fig. 1 of Branch 1987) and, simultaneously, the higher-excitation lines of the other ions like Ca II.

5. DISCUSSION

In SNe Ia, the energy of the initial explosion gained through thermonuclear fusion is used up by the adiabatic expansion of the ejecta (e.g., Leibundgut & Pinto 1992), whereas the light curve is powered by the decay of radioactive 56Ni and 56Co. It is also believed that there is a direct link between the mass of the 56Ni produced during the explosion and the peak bolometric luminosity (see, e.g., Arnett, Branch, & Wheeler 1985; Höflich et al. 1996). The observed low optical luminosity of SN 1998de is indicative of its bolometric luminosity for the following reasons: the peak of the energy distribution of SN 1998de lies in the optical part of the spectrum, thus we can be confident that the low observed optical luminosity translates into a similarly low bolometric luminosity. Furthermore, there is no plausible way to have a large UV excess, nor is there evidence for a large amount of dust, which could have reprocessed the optical photons of SN 1998de to provide a significant infrared excess.

Therefore, we can conclude that the mass of the synthesized nickel was smaller in SN 1998de than in normal SNe Ia. M97 derive a value of ~0.07 M⊙ of synthesized 56Ni for SN 1991bg, which agrees well with the original estimate of Ruiz-Lapuente et al. (1993) of 0.05–0.1 M⊙ and which is a factor of 4–8 smaller than in normal SNe Ia. We could expect that similar amounts of nickel have been produced in both SN 1991bg and SN 1998de, as both SNe exhibit similar absolute magnitudes in all filters. However, spectral synthesis calculations and bolometric light curves are necessary for obtaining a definitive value for the nickel mass.

On the other hand, there are a number of indications that suggest that SN 1998de might have experienced a slightly more powerful explosion than SN 1991bg did. Among these are the marginally slower decline of the light curves in the V, R, and I bands and the offset of the color curves toward the blue. The fact that SN 1998de appears to show the same luminosities when compared with SN 1991bg (on the same distance scale) is only mildly inconsistent with the other pieces of evidence.

The models which have been proposed to explain the physics of SNe Ia in the last 30 years can be divided into two main categories: those that describe different explosion mechanisms with the same progenitor system, and those that propose different systems as the reason for the heterogeneity of SNe Ia and in particular as production sites of subluminous SNe Ia. Despite the partial success of various models (see reviews by, e.g., Woosley & Weaver 1986; Wheeler & Harkness 1990; Branch et al. 1995; Livio 2000; Hillebrandt & Niemeyer 2000), no general consensus about the exact character of the explosion mechanism and the evolutionary track that leads to the SN Ia event has yet been reached.

Höflich, Khokhlov, & Wheeler (1995) used the pulsating class of delayed detonation models to establish the principle
that Chandrasekhar-mass C-O white dwarfs give a common explosion mechanism accounting for both normal and subluminous SNe Ia, with SN 1991bg as their example for the latter group. However, as T96 correctly point out, their model requires a large reddening for SN 1991bg \([E(B-V) = 0.30 \text{ mag}]\) in order to harmonize the theoretical luminosity with the observed value, while observations indicate a much smaller value close to zero (F92; L93; T96). Also, the decline rates of their SN 1991bg models are similar to those of their normal SN Ia models, while that of SN 1991bg is observed to be much faster.

As mentioned by F92 and others, an alternative scenario for subluminous SNe Ia might involve ejecta with mass appreciably smaller than the Chandrasekhar limit that would account for several of the peculiar features of SN 1998de. The trapping of gamma rays produced by the decay of \(^{56}\text{Ni}\) and \(^{56}\text{Co}\) would be less effective owing to the low column depth of the ejecta, thus leading to the rapid decline in the observed BVRI light curves after maximum light and possibly to the low optical luminosity. Also, low-mass ejecta expanding at only a slightly slower velocity than in normal SNe Ia would allow the photosphere to recede more quickly than usual, revealing the deeper layers and giving rise to the early emergence of the nebular spectrum.

The decline in photospheric expansion velocity from ~13,000 km s\(^{-1}\) at \(t = -6 \text{ days}\) (Garnavich et al. 1998) to 7080 km s\(^{-1}\) at \(t = 31 \text{ days}\) might be consistent with that of SN 1991bg, which showed an expansion velocity of ~7000 km s\(^{-1}\) at \(t = 27 \text{ days}\). Unfortunately, there are no other data points available for SN 1998de, especially since photospheric velocities are not defined during the nebular phase (i.e., for our last two spectra), and no premaximum spectra are available for SN 1991bg.

The consistently small velocity observed in SN 1991bg was interpreted by T96 as a possible indication that complete nuclear burning was confined to the innermost regions. Other phenomena which are thought to support this conclusion are the high abundance of oxygen (suggested by the \([\text{O} \text{ i}] \lambda 5577 \text{ and O i } \lambda 7774 \text{ lines}]\) left over from the progenitor (T96; M97) and the narrow \([\text{Co} \text{ iii}]\) emission at \(5908 \text{ Å}\). Using the presence and strength of those features as observed in SN 1998de, we might infer that the inner region of complete burning was somewhat larger in SN 1998de than in SN 1991bg; indicators include the weaker appearance of \([\text{O} \text{ i}] \lambda 7774 \text{ and the somewhat broader } [\text{Co} \text{ iii}] \text{ emission at } 5900 \text{ Å} \text{ in } \text{SN 1998de}].\) Furthermore, the hypothesis that SN 1998de might have experienced a slightly more powerful explosion than SN 1991bg did is consistent with this model. The red color of both SNe 1998de and 1991bg seems to implicate a low excitation temperature which gives rise to the Ti ii trough found at the blue end of the spectrum without requiring an overabundance of titanium.

Here we briefly review some of the scenarios proposed to explain the ejection of a sub-Chandrasekhar envelope. Livne (1990), Woosley & Weaver (1994), and Höflich & Khokhlov (1996) suggest that the progenitor itself has a mass below the Chandrasekhar limit. According to their models, a sub-Chandrasekhar-mass C-O white dwarf detonates because of the ignition of an outer He shell accumulated on top of it. Their predictions include a lower luminosity, a lower production rate of nickel, and an overabundance of titanium. In addition, the observed light curves can be adequately reproduced with this model. The absence of unburned He in the spectra might be explained by the low excitation temperatures present. On the other hand, they predict bluer colors at maximum brightness, while SNe 1991bg and 1998de are very red at that phase, as well as an outer Ni shell, which has not been observed in any of the subluminous SNe Ia. Moreover, they do not account for the outer oxygen shell.

Another possibility might be a double-degenerate system of intermediate-mass C-O white dwarfs that merge, giving rise to the disruption of the less massive star, followed by the formation of a thick, hot accretion disk around the more massive companion and the subsequent explosion of the remaining white dwarf when it reaches the Chandrasekhar limit (e.g., Iben & Tutukov 1984; Webbink 1984). As a consequence, only a small mass of \(^{56}\text{Ni}\) would be produced, and there would be a mixture of burned and unburned material as observed in SN 1991bg and SN 1998de. However, the outcome of such a coalescence is still not completely understood; there are strong indications that it may rather lead to accretion-induced collapse forming a neutron star than to an SN event (see, e.g., Saio & Nomoto 1985, 1998; Woosley & Weaver 1986; Mochkovitch & Livio 1990; Mochkovitch, Guerrero, & Segretain 1997).

Unfortunately, none of the proposed models unambiguously emerges as the preferred candidate for explaining subluminous SNe Ia, since each of the models appears beset by some problems as discussed above. Detailed studies of more subluminous SNe are needed to provide additional constraints for the models. Indeed, the ongoing efforts of LOSS to conduct photometric follow-up observations of recently discovered subluminous SNe Ia promise to contribute significantly; the results will be discussed by W. D. Li et al. (2001, in preparation).

6. Conclusions

We have presented a set of photometric and spectroscopic observations of the recent SN 1998de, which reveal it to be an intrinsically faint SN Ia, similar to, but not identical with, SN 1991bg. Similarities include (1) the intrinsically low luminosity; (2) the remarkably red colors near maximum; (3) the narrow peak in all bands; (4) the rapid and monotonic decline of the light curves, including in the I band; (5) the strong Ti ii absorption lines throughout all observed epochs; (6) the early transition to a nebular spectrum; and (7) the strong [Ca ii] emission lines at late times. The very good coverage and high quality of the BVRI light curves make SN 1998de a defining template for subluminous SNe Ia, superior to the conventional template SN 1991bg, and clearly establish SN 1998de as a fast riser.

Whereas the B passband provides the best early-time match
between SN 1991bg and SN 1998de, the deviations in both light curves and spectra between the two SNe Ia seem to increase toward longer (redder) wavelengths. Features of SN 1998de that distinguish it from SN 1991bg include (1) a plateau phase (or a possible second maximum) in the \( I \) band, very shortly after the first maximum; (2) a slower decline of the light curves in the \( V, R \), and \( I \) bands; (3) slightly bluer colors at intermediate phases; (4) the absence of the conspicuous Na i D absorption found at 5700 Å in the spectra of SN 1991bg; and (5) the evolution of a region (6800–7600 Å) in the spectra of SN 1998de from featureless to feature-rich. Our comparison of SN 1998de and SN 1991bg may imply that subluminous SNe Ia are not fully described as a one-parameter \( [\Delta m_{15}(B)] \) family. The somewhat slower decline rates and bluer colors, combined with the evidence that the region of complete burning was larger in SN 1998de than in SN 1991bg, suggest that SN 1998de might have experienced a slightly more powerful explosion than SN 1991bg did.

The observed peculiarities of SN 1998de (and of SN 1991bg) might be explained in terms of ejecta with a mass smaller than that found in normal SNe Ia. However, at this time Chandrasekhar-mass models seem to provide an equally acceptable explanation.

Our analysis strengthens the conclusion that SN 1991bg was not a unique event, as already proposed by studies of several other intrinsically dim SNe Ia. Further conclusions to be drawn—besides the insights into the intrinsic workings of SNe Ia—concern the implications of our observations for the calibrated-candle assumption of SNe Ia and for their usage as cosmological distance indicators. We propose that intrinsically subluminous SNe Ia should be identified in samples of SNe Ia used for cosmological purposes, with the Ti ii trough at the blue end of the spectrum and the absence of a clear secondary maximum in the rest-frame \( I \) band as possible criteria. It is advisable that the standard calibration methods be applied with caution on such objects; for example, the “snapshot” method of deriving distances of SNe Ia (Riess et al. 1998b) currently assumes that the objects are normal.

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REFERENCES

Arnett, W. D., Branch, D., & Wheeler, J. C. 1985, Nature, 314, 337
Barbon, R., Benetti, S., Cappellaro, E., Rosino, L., & Turatto, M. 1990, A&A, 237, 79
Bessell, M. S. 1999, PASP, 111, 1426
Branch, D. 1987, ApJ, 320, L121
———. 1998, ARA&A, 36, 17
Branch, D., Drucker, W., & Jeffery, D. J. 1988, ApJ, 330, L117
Branch, D., Fisher, A., & Nugent, P. 1993, AJ, 106, 2383
Branch, D., Livio, M., Yungelson, L. R., Boffi, F. R., & Baron, E. 1995, PASP, 107, 1019
Branch, D., & Tammann, G. A. 1992, ARA&A, 30, 359
Cousins, A. W. J. 1981, South African Astron. Obs. Circ., 6, 4
de Vaucouleurs, G., de Vaucouleurs, A., Corwin, H. G., Jr., Buta, R. J., Paturel, G., & Fouqué, P. 1991, Third Reference Catalogue of Bright Galaxies (New York: Springer)
Eder, J., Giovanelli, R., & Haynes, M. P. 1991, AJ, 102, 572
Filippenko, A. V. 1997, ARA&A, 35, 309
Filippenko, A. V., Porter, A. C., Sargent, W. L. W., & Schneider, D. P. 1986, AJ, 92, 1341
Filippenko, A. V., et al. 1992a, ApJ, 384, L15
———. 1992b, AJ, 104, 1543 (F92)
Ford, C. H., et al. 1993, AJ, 106, 1101
Garcia, A. M. 1993, A&AS, 100, 47
Garnavich, P., Jha, S., & Kirshner, R. 1998, IAU Circ. 6980
Hamuy, M., Phillips, M. M., Suntzeff, N. B., Schommer, R. A., Maza, J., & Avilés, R. 1996a, AJ, 112, 2391
Hamuy, M., Phillips, M. M., Suntzeff, N. B., Schommer, R. A., Maza, J., Smith, R. C., Lira, P., & Avilés, R. 1996b, AJ, 112, 2438
Hamuy, M., Phillips, M. M., Wells, L. A., & Maza, J. 1993, PASP, 105, 787
Hamuy, M., et al. 1994, AJ, 108, 2226
Harkness, R. P., & Wheeler, J. C. 1990, in Supernovae, ed. A. G. Petschek (New York: Springer), 1
Hillebrandt, W., & Niemeyer, J. C. 2000, ARA&A, 38, 191
Höflich, P., & Khokhlov, A. M. 1996, ApJ, 457, 500
Höflich, P., Khokhlov, A. M., & Wheeler, J. C. 1995, ApJ, 444, 831
Höflich, P., Khokhlov, A. M., & Wheeler, J. C., Phillips, M. M., Suntzeff, N. B., & Hamuy, M. 1996, ApJ, 472, L81
Huchra, J. P., Vogeley, M. S., & Geller, M. J. 1999, ApJS, 121, 287
Iben, I., Jr., & Tutukov, A. V. 1984, ApJS, 54, 335
Jeffery, D. J., Leibundgut, B., Kirshner, R. P., Benetti, S., Branch, D., & Sonneborn, G. 1992, ApJ, 397, 304
Jha, S., et al. 1999, ApJS, 125, 73
Johnson, H. L., Mitchell, R. I., Iriarte, B., & Wisniewski, W. Z. 1966, Commun. Lunar Planet. Lab., 4, 99
Kirshner, R. P., et al. 1993, ApJ, 415, 589
Kraan-Korteweg, R. C. 1986, A&AS, 66, 255
Landolt, A. U. 1992, AJ, 104, 340
Leibundgut, B., & Pinto, P. A. 1992, ApJ, 401, L49
Leibundgut, B., et al. 1993, AJ, 105, 301 (L93)
Li, W. D., Filippenko, A. V., & Riess, A. G. 2000b, in Cosmic Explosions, ed. S. S. Holt & W. W. Zhang (New York: AIP), 91
Li, W. D., et al. 2000a, in Cosmic Explosions, ed. S. S. Holt & W. W. Zhang (New York: AIP), 103
Li, W. D., et al. 2000a, in Cosmic Explosions, ed. S. S. Holt & W. W. Zhang (New York: AIP), 91
Livio, M., 2000, in Type Ia Supernovae: Theory and Cosmology, ed. J. C. Niemeyer & J. W. Truran (Cambridge: Cambridge Univ. Press), 33
Livne, E. 1990, A&A, 237, 79
Mazzali, P. A., Chugai, N., Turatto, M., Lucy, L. B., Danziger, I. J., Cappellaro, E., Della Valle, M., & Benetti, S. 1997, MNRAS, 284, 151 (M97)
Miller, J. S., & Stone, R. P. S. 1993, Lick Obs. Tech. Rep. 66 (Santa Cruz: Lick Obs.)
Mochkovitch, R., Guerrero, J., & Segretain, L. 1997, in Thermonuclear Supernovae, ed. P. Ruiz-Lapuente, R. Canal, & J. Isern (Dordrecht: Kluwer), 187
Mochkovitch, R., & Livio, M. 1990, A&A, 236, 378
Modjaz, M., et al. 1998, IAU Circ. 6977
Nugent, P., Phillips, M., Baron, E., Branch, D., & Hauschildt, P. 1995, ApJ, 455, L147
Oke, J. B., & Gunn, J. E. 1983, ApJ, 266, 713
Pagel, B. E. J. 1997, Nucleosynthesis and Chemical Evolution of Galaxies (Cambridge: Cambridge Univ. Press)
Perlmuter, S., et al. 1997, ApJ, 483, 565
———. 1999, ApJ, 517, 565
Phillips, M. M. 1993, ApJ, 413, L105
Phillips, M. M., Wells, L. A., Suntzeff, N. B., Hamuy, M., Leibundgut, B., Kirshner, R. P., & Foltz, C. B. 1992, AJ, 103, 1632
Phillips, M. M., et al. 1999, AJ, 118, 1766
Richmond, M. W., Treffers, R. R., & Filippenko, A. V. 1993, PASP, 105, 1164
Richmond, M. W., et al. 1995, AJ, 109, 2121
Riess, A. G. 2000, in Cosmic Flows Workshop, ed. S. Courteau & J. Willick (San Francisco: ASP), 80
Riess, A. G., Nugent, P., Filippenko, A. V., Kirshner, R. P., & Perlmutter, S. 1998b, ApJ, 504, 935
Riess, A. G., Press, W. H., & Kirshner, R. P. 1995, ApJ, 445, L91
———. 1996, ApJ, 473, 88
Riess, A. G., et al. 1998a, AJ, 116, 1009
———. 1999a, AJ, 117, 707
———. 1999b, AJ, 118, 2675

Ruiz-Lapuente, P., Cappellaro, E., Turatto, M., Gouiffes, C., Danziger, I. J., Della Valle, M., & Lucy, L. B. 1992, ApJ, 387, L33
Ruiz-Lapuente, P., et al. 1993, Nature, 365, 728
Saha, A., Labhardt, L., & Prosser, C. 2000, PASP, 112, 163
Saha, A., Sandage, A., Labhardt, L., Schwengeler, H., Tammann, G. A., Panagia, N., & Macchetto, F. D. 1995, ApJ, 438, 8
Saio, H., & Nomoto, K. 1985, A&A, 150, L21
———. 1998, ApJ, 500, 388
Savage, B. D., & Mathis, J. S. 1979, ARA&A, 17, 73
Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, ApJ, 500, 525
Schmidt, B. P., et al. 1993, AJ, 105, 2236
Stetson, P. B. 1987, PASP, 99, 191
Suntzeff, N., et al. 1999, AJ, 117, 1175
Tonry, J. L., Blakeslee, J. P., Ajhar, E. A., & Dressler, A. 2000, ApJ, 530, 625
Treffers, R. R., Peng, C. Y., Filippenko, A. V., & Richmond, M. W. 1997, IAU Circ. 6627
Tripp, R. 1998, A&A, 331, 815
Turatto, M., Piemonte, A., Benetti, S., Cappellaro, E., Mazzali, P. A., Danziger, I. J., & Patat, F. 1998, AJ, 116, 2431
Turatto, M., et al. 1996, MNRAS, 283, 1 (T96)
Vaughn, T. E., Branch, D., Miller, D. L., & Perlmutter S. 1995, ApJ, 439, 558
Vettolani, G., & Baiesi Pillastrini, G. C. 1987, A&A, 175, 9
Wade, R. A., & Horne, K. 1988, ApJ, 324, 411
Webbink, R. F. 1984, ApJ, 277, 355
Wells, L. A., et al. 1994, AJ, 108, 2233
Wheeler, J. C., & Harkness, R. P. 1990, Rep. Prog. Phys., 53, 1467
Woosley, S. E., & Weaver, T. A. 1986, ARA&A, 24, 205
———. 1994, ApJ, 423, 371
Zehavi, I., Riess, A. G., Kirshner, R. P., & Dekel, A. 1998, ApJ, 503, 483