Constructing population of initial university timetable: design and analysis

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Article Info

ABSTRACT

The construction of population of initial timetable is an essential stage in population-based metaheuristic approach for solving curriculum-based university course timetabling problem because it may impact the quality of the final timetable. This paper presents population of initial timetable construction approach in curriculum-based course timetabling problem by using the graph heuristics to determine the sequential order of courses/lectures to be assigned in the timetable. The graph heuristics were implemented as single and combination of two heuristics. The courses in curriculum-based university course timetabling problem that was organized based on the heuristics setting will be repeatedly assigned to valid empty slots while fulfilling all the hard constraints. If a course is unable to be assigned to whichever slots because of no more valid empty slots, it will be inserted into the unscheduled courses/lectures list. The unscheduled courses/lectures list will be assigned later to the timetable using several procedures executed in a sequence. The approaches were tested on the ITC2007 instances and the results were analyzed with some statistical tests to determine the best setting of heuristics in the construction approach. The result shows that the construction approach with combination of largest degree followed by saturation degree heuristic, generate the maximum number of population of initial timetables. The result from this study can be used in the improvement stage of metaheuristic algorithm that uses population-based approach.

Keywords:
Curriculum based university course timetabling
Graph heuristics
Initial solution
Population based metaheuristic
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1. INTRODUCTION

The curriculum-based university course timetabling (CBCCT) which is produced based on university curricula, assign the lectures (came from courses) to suitable classrooms and timeslots. The allocation is established based on a set of constraints and designated on a weekly basis. The entities involved in CBCCT includes Days, Timeslots, Periods, Rooms, Curricula, Courses and Teachers [1]. Days are quantity of teaching days in a week. Timeslots are amount of slots in a day. Periods are amount of combination between Days and Timeslots. Rooms are halls with number of seats. Curricula is a set of courses in which any pair of courses in the set have students in common. Courses are consists of number of lectures and each lecture is associated to a Teacher. The conflict between courses in CBCCT are produced based on the Curricula.

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Allocating the lectures to classrooms and periods is determined on satisfying several constraints, so that a feasible timetable can be produced. A feasible timetable is a timetable with no hard constraint violation, but perhaps contain soft constraint violation. The soft constraint violation is showed by amount of penalty cost. Therefore, solving CBCTT problem basically is to decrease that amount of penalty cost in a feasible timetable. This study adopts the hard and soft constraints used in [2]. The hard constraints are lectures, room occupancy, conflicts and availability, while the soft constraints are room capacity, minimum working days, curriculum compactness and room stability. The detail of each constraint is described in Table 1. The quality of solution is calculated as the total penalties of the soft constraints: room capacity + minimum working days + curriculum compactness + room stability.

| Type               | Constraints       | Description                                                                 |
|--------------------|-------------------|-----------------------------------------------------------------------------|
| Hard constraints   | Lectures          | All lectures must be scheduled to a different period and a room              |
|                    | Room occupancy    | Two lectures cannot be assigned to the same room and the same period         |
|                    | Conflicts         | Lectures in the same curriculum or taught by the same teacher must be assigned to separate periods |
|                    | Availability      | If the teacher of a course is not available at a certain period, then no lectures of the course can be allocated to that period |
| Soft constraints   | Room capacity     | The quantity of students for each lecture must be fewer or equivalent to the volume of the rooms |
|                    | Minimum working days | The lectures of each course should span thru a given number of days         |
|                    | Curriculum compactness | Lectures of courses of the same curriculum should be in contiguous periods |
|                    | Room stability    | All lectures of a specific course are supposed to be allocated to the same room |

The stages in the process of solving the CBCTT problem usually comprise of the construction and the improvement phases [3]. In the construction stage, an empty timetable will be progressively inserted by a lecture one by one in repetition and at the same time the violation of the hard constraint is also inspected. At the end of this stage, an initial timetable with no hard constraint violation will be produced. However, the initial timetable may have many soft constraint violation. In the improvement stage, the soft constraint violation in the initial timetable will be iteratively decreased to a minimum or zero value. The aim of this stage is to produce a better and reliable timetable.

For the construction stage, the sequential constructive algorithm is widely studied and employed in university timetabling problem [4-10]. Sequential constructive algorithm uses a strategy to select the next event and construct the full timetable by assigning the events one at a time (sequentially) to a selected timeslot. The strategy is to order the events that are not yet scheduled according to the difficulties in scheduling them into a feasible timeslot (without violating any hard constraints) [11]. A number of commonly used strategies have been adopted from the graph coloring problem [11] such as least saturation degree (SD) - in each step of the timetable construction, an event which has the least number of available slots in the timetable constructed so far is selected, largest degree (LD) - events are ordered in descending manner by the number of conflicts they have with other events, largest weighted degree (LW) - events are ordered decreasing by the total number of students in conflict with other event, largest enrolment (LE) - events are ordered decreasing by the total number of student enrolments, largest color degree (CD) - events are ordered decreasing in terms of the other events that are in conflict and have already been scheduled in the timetable, and random ordering (RO) - events that are not yet scheduled are ordered randomly.

In the context of the CBCTT benchmark data sets, the graph coloring based heuristic orderings has been implemented mostly using SD [12-15] and LD [16, 17]. It was observed that the use of the graph heuristic alone in single phase led to infeasible timetable for some problem instances [15].

For the improvement stage, the improvement process is an iterative process in which the initial timetable is modified at each step in order to minimize the soft constraint violation in the timetable. The most common approach for the iterative improvement is metaheuristic methods [18]. There are two types of methods in metaheuristic such as local search-based methods and population-based methods [18]. Local search-based methods used in solving CBCTT include simulated annealing (SA) [19, 20], great deluge (GD) [21] and tabu search (TS) [22] require only one initial timetable in order to proceed with the improvement process. In the other hand, population-based methods used in solving CBCTT include ant colony optimization (ACO) [23], artificial bee colony (ABC) [15, 24], genetic algorithm (GA) [25, 26] and harmony search algorithm (HSA) [27, 28] require population of initial timetable in its improvement process. To produce a population of initial timetable requires algorithm that can produce multiple feasible timetables and these timetables must also be diverse. This process is a vital stage because it can influence the convergence speed i.e. process of decreasing the soft constraint violation and also the quality of the final timetable [29].
Hence, this study implemented an events assignment procedure that used different graph heuristics simultaneously in two phase approach. The phases consists of typical events assignment procedure in the first phase and also procedure for unassigned events in the second phase.

This study was able to construct population of initial timetable for various CBCTT data instances, therefore, generally, this study can contribute to the metaheuristic improvement approach. Specifically, this study can contribute to population-based methods of metaheuristic that use population of initial timetables such as ant colony optimization (ACO), artificial bee colony (ABC), genetic algorithm (GA), and harmony search algorithm (HSA).

2. RESEARCH METHOD

The proposed construction method is shown in Figure 1. The first step in the method is to determine the sequential order of courses/lectures to be scheduled using the combination of graph heuristics. From six different graph heuristics described in [11], this study investigates only three type of the heuristics. These heuristics have been selected because they are the most commonly used graph heuristics and have generated feasible initial timetables for all data instances of CBCTT [14, 16, 17]. The graph heuristics are LD, LW, and SD.

![Figure 1. Approach for constructing population of initial solution](image)

The courses were ordered using single heuristic, and a combination of two heuristics. The ordering method is identified by the following label of combination(s): L (LD), W (LW), S (SD), LS (LD with SD), WS (LW with SD), SL (SD with LD), and SW (SD with LW). LW is a heuristic that orders the events by the descending number of students involved in conflicts. This heuristic already contains the LD (descending number of conflicts) heuristic, therefore there is no combination between LD and LW.

In the second step, each of the lectures/courses which is previously arranged based on the heuristics setting will be randomly and iteratively allocated to valid empty slots while satisfying all the hard constraints. If a lecture is unable to be assigned to any slots because of no more valid empty slots, it will be inserted into the unscheduled lectures list. The unscheduled lectures/courses list will be assigned later to the timetable using several methods executed in a sequence.

The unassigned lecture assignment procedures consist of nine procedures. Each procedure tries to assign all the unassigned lectures to a valid timeslot. If there are more unassigned lectures, the next procedures will be executed. This implies that the current procedures are not able to assign some lectures; therefore, the next procedure will be attempted.

Procedure 1: Randomly assign the unassigned lecture to the available slot that is empty, free from conflict and conform to the unavailability constraints.

Procedure 2: Find an available slot that is empty and conforms to the unavailability constraints but have one lecture, which is in conflict with the unassigned lecture. As shown in Figure 2, the scheduled
lecture, 13, that contributed to the conflict, which is located in the same period (Slot i) with the available slot will be moved to another slot (Slot j) that is empty (the properties of suitable room, free from conflict, and conforming to the unavailability constraints are also maintained in this movement). This movement makes the available slot free from conflict and the unassigned lecture that is 11 can be scheduled in the available slot in Room 1.

**Figure 2. Graphic Illustration for Procedure 2**

Procedure 3: Find an available slot that is not empty (there is a lecture already scheduled to it) but the slot is appropriate in terms of free from conflict and conforming to the unavailability constraints with the unassigned lecture. The scheduled lecture, i.e. 6, will be moved to another slot (Slot j) that is empty (the properties of suitable room, free from conflict, and conforming to the unavailability constraints are also maintained in this movement). The unassigned lecture that is 11 can then be scheduled in the slot (Slot i) that is empty. Figure 3 shows the graphic illustration for this step.

**Figure 3. Graphic Illustration for Procedure 3**

Procedure 4: Find an available slot that is not empty (there is a lecture already scheduled to it) and conforms to the unavailability constraints but have one conflict with the unassigned lecture. As shown in Figure 4, the scheduled lecture, 13 that contributes to the conflict which is located in the same period (Slot i)
with the available slot will be moved to another slot (Slot j) that is empty (the properties of suitable room, free from conflict, and conforming to the unavailability constraints are also maintained in this movement). This movement makes the available slot free from conflict. The next step is to move the scheduled lecture, 6 that is located in the available slot into the empty slot left by scheduled lecture, 13 that contributes to the conflict (the properties of suitable room, free from conflict, and conforming to the unavailability constraints are also maintained in this movement). Finally, the unassigned lecture 11 can be scheduled in the available slot.

![Graphic Illustration for Procedure 4](image)

Figure 4. Graphic Illustration for Procedure 4

Procedure 5 until Procedure 8 will use the same procedure with Procedure 1 until Procedure 4 respectively. The difference with Procedure 5 to Procedure 8 is that the selection of available slot does not conform to unavailability constraints. This approach is used to provide alternative in the process of satisfying the hard constraints only since the unavailability constraints are considered to be the soft constraints. Procedures 5 to 8 relax the unavailability constraints while satisfying the hard constraints. In other words, the resulting timetable is still feasible but with higher number of soft constraints.

Procedure 9 is executed in which each scheduled slot in the timetable will be moved to an available empty slot (the properties of suitable room, free from conflict, and conforming to the unavailability constraints are also maintained in this movement). This step will change the overall timetable which contributes to provide different available slots in the next inner iteration.

Procedures 1 to 9 are repeated with different available slots (because Procedure 9 changes the overall slot in the timetable) from previous iterations. This procedure is iterated up to 20 times. This number of iterations is chosen because based on earlier experiments, normally, a feasible solution is found within 20 iterations.

After all the lectures are scheduled, the timetable will be validated. If the timetable is feasible, the algorithm stores the timetable and starts another courses (lectures) assignment procedure with another random seed. Otherwise, the present timetable will be eliminated and another courses (lectures) assignment procedure will be executed with a different random seed. The procedure of courses (lectures) assignment will be iterated for 50 times so that a maximum of 50 feasible timetables can be generated.

3. RESULTS AND ANALYSIS

The proposed construction approach was developed using C++ language and experimented using computer with an Intel Core i7 with 3.4 GHz processor. The experiment was carried out using six problem instances (comp01, comp02, comp03, comp04, comp05 and comp06) from International Timetabling Competition (ITC) 2007 available at http://tabu.diegm.uniud.it/ctt website. The proposed construction approach with several graph heuristic settings were performed for each problem instance, without imposing a time limit as a stopping condition. For each problem instance, the total number of feasible solutions of over 50 iterations will be produced.
The results of individual graph heuristic of L, W and S and combination of graph heuristics of LS, WS, SL and SW are shown in Tables 2 and 3 respectively. In the tables, TOT represents the total number of feasible initial solutions produced over 50 iterations, while MIN and MAX denote as the minimum cost and maximum cost of soft constraints violation that is produced.

Table 2. Results of Feasible Initial Solution of Single Heuristic

| Problem Instances | L  | W  | S  | TOT | MIN | MAX |
|-------------------|----|----|----|-----|-----|-----|
| comp01            | 50 | 346| 646| 50  | 365 | 900 |
| comp02            | 50 | 781| 1409| 50  | 757 | 1586|
| comp03            | 49 | 682| 1193| 50  | 705 | 1277|
| comp04            | 50 | 708| 843 | 50  | 696 | 987 |
| comp05            | 2  | 1625| 2027 | 2  | 1405| 1769|
| comp06            | 50 | 957| 1276| 50  | 952 | 1595|

Table 3. Results of Feasible Initial Solution of Combination Heuristic

| Problem Instances | LS | WS | SL | SW  | TOT | MIN | MAX |
|-------------------|----|----|----|-----|-----|-----|-----|
| comp01            | 50 | 330| 569| 50  | 326 | 690 |
| comp02            | 50 | 769| 1345| 50  | 762 | 1424|
| comp03            | 50 | 702| 881 | 50  | 701 | 1209|
| comp04            | 50 | 694| 831 | 50  | 705 | 934 |
| comp05            | 4  | 1466| 1890 | 2  | 1313| 1750|
| comp06            | 50 | 947| 1448| 50  | 964 | 1473|

Tables 2 and Table 3 show the results of the construction approach with all graph settings for all problem instances. Over 50 iterations, the construction approach is able to produce 50 feasible initial solution for all problem instances except for problem instances comp05. The highlighted row shows that the construction approach with all graph settings produce less then 10 percent of feasible initial solutions over 50 iterations for comp05. This is probably because of the complexity of the problem instance comp05.

Therefore, for the purpose of comparison, the construction approach will be executed with 10 runs on the problem instance of comp05 in order to investigate the best setting of graph heuristic used in the construction approach. Table 4 shows the number of feasible initial solutions of comp05 problem instance produced over 50 iterations for each graph heuristic setting with 10 runs.

Table 4. Number of Feasible Initial Solutions Produced over 50 Iterations for 10 runs on Comp05

| Run | L   | W   | S   | LS  | WS  | SL  | SW  |
|-----|-----|-----|-----|-----|-----|-----|-----|
| 1   | 1   | 2   | 1   | 3   | 2   | 7   | 3   |
| 2   | 3   | 4   | 1   | 2   | 1   | 2   | 5   |
| 3   | 4   | 0   | 1   | 4   | 4   | 2   | 2   |
| 4   | 4   | 0   | 0   | 2   | 0   | 3   | 2   |
| 5   | 1   | 3   | 1   | 2   | 1   | 3   | 5   |
| 6   | 6   | 3   | 2   | 4   | 1   | 2   | 2   |
| 7   | 1   | 3   | 1   | 2   | 2   | 3   | 6   |
| 8   | 0   | 1   | 2   | 2   | 1   | 0   | 3   |
| 9   | 0   | 4   | 1   | 1   | 0   | 3   | 3   |
| 10  | 1   | 2   | 1   | 2   | 3   | 3   | 4   |
| TOTAL| 22  | 22  | 10  | 24  | 15  | 28  | 35  |

A statistical analysis, i.e. single factor analysis of variance (ANOVA) is carried out to inspect whether each setting has a significant difference in producing a number of initial solutions. A single factor ANOVA is used to test the null hypothesis, $H_0$ ($H_0$: The means of several groups are all equal). The hypothesis for this analysis, which is:

$H_0$: $\mu_L = \mu_S = \mu_W = \mu_{LS} = \mu_{WS} = \mu_{SL} = \mu_{SW}$

$H_1$: Not all the means are equal.
was performed at 5% significance level. The single factor ANOVA produced result called as p-value which consisted of probability number ranging from zero to one. The p-value is used to measure the difference in population means and used as an evidence to reject or accept the null hypothesis. Table 5 shows the result of ANOVA. The p-value for the hypothesis test is 0.007. This value is less than the specified significance level of 0.05, therefore $H_0$ is rejected. At 5% significance level, there is a significant difference between the graph heuristics settings in producing the feasible initial solutions.

Table 5. Result of ANOVA for Measuring the Different in the Graph Heuristics Settings

| Source of Variation | SS        | df | MS      | F        | $P$-value | F crit |
|---------------------|-----------|----|---------|----------|-----------|--------|
| Between Groups      | 40.14286  | 6  | 6.690476| 3.287832 | 0.007059  | 2.246408|
| Within Groups       | 128.2     | 63 | 2.034921|          |           |        |
| Total               | 168.3429  | 69 |         |          |           |        |

However, the ANOVA analysis does not show where the difference lies. Another analysis, i.e. t-test, is carried out to test the null hypothesis that the means of two populations are equal. In this case, each setting is paired and the t-test value of each pair is produced as shown in Table 6. At 5% significance level, null hypothesis, i.e. both paired settings have no significant difference, is rejected for W:S (0.03), W:WS (0.001), W:SW (0.01), S:LS (0.01), S:SL (0.02), S:SW (0.001), and WS:SW (0.01). In other words, these seven pairs of graph heuristic settings have significant difference in producing the initial solutions.

Table 6. Result of T-test for Each Pair of Graph Heuristic Settings

| L | W | S | LS | WS | SL | SW |
|---|---|---|----|----|----|----|
| 1 | 0.09634 | 0.66178 | 0.297715 | 0.496102 | 0.201495 |
| 2 | 0.036787 | 0.764041 | 0.001005 | 0.404755 | 0.013276 |
| 3 | 0.001323 | 0.343436 | 0.023856 | 0.001617 |
| 4 | 0.121232 | 0.533786 | 0.128623 |
| 5 | 0.089781 | 0.01682 |
| 6 | 0.343436 | 0.034336 |

Based on the total number of feasible initial solutions produced as shown in Table 4 earlier and Table 6, the overall best setting(s) can be determined as listed in Table 7 by shortlisting the best settings in each pair. In pair 1 and pair 2, the graph heuristic W is determined as the best so far because it has greater total number of feasible initial solutions compared to graph heuristic S and WS. However, when compared to pair 3, graph heuristic W is no longer considered the best setting because graph heuristic SW has greater total number of feasible initial solutions compared to graph heuristic W. In pair 4 and pair 5, LS and SL are both better than their pair and each of them is included together with SW as the best graph heuristic settings so far. In pair 6 and pair 7, it seems that SW has better total number of feasible initial solutions compared to their pair. At the end, the best overall settings consist of SW, LS and SL.

Table 7. Shortlisting the Pairs of Graph Heuristic to Determine the Best Graph Heuristic Setting(s)

| No | Pair of Settings | Total Number of Initial Solutions | Best setting in pair | Overall Best setting |
|----|------------------|----------------------------------|----------------------|---------------------|
| 1  | W : S            | 22:10                            | W                    | W                   |
| 2  | W : WS           | 22:15                            | W                    | W                   |
| 3  | W : SW           | 22:35                            | SW                   | SW                  |
| 4  | S : LS           | 10:24                            | LS                   | SW                  |
| 5  | S : SL           | 10:28                            | SL                   | SW, LS              |
| 6  | S : SW           | 10:35                            | SW                   | SW, LS, SL          |
| 7  | WS : SW          | 15:35                            | SW                   | SW, LS, SL          |

To determine the best setting among SW, LS and SL, another 10 runs of comp05 using these settings are carried out. The total number of initial solutions produced over 50 iterations for 20 runs of SW, LS and SL is shown in Table 8. It is observed that graph heuristics SW and SL have the probability of producing zero (0) feasible initial solutions in Run 18 and 8 respectively. Based on this, it can be concluded that the graph heuristic LS is the best setting compared to SW and SL.
Table 8. Feasible Initial Solutions Produced by SW, LS and SL over 50 Iterations on Comp05

| Run | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
|-----|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|
| SW  | 3 | 5 | 2 | 2 | 5 | 2 | 6 | 3 | 3 | 4 | 3 | 4 | 1 | 2 | 1 | 4 | 2 | 0 | 3 | 2 |
| LS  | 3 | 2 | 4 | 2 | 2 | 4 | 2 | 2 | 1 | 2 | 3 | 4 | 3 | 2 | 4 | 5 | 3 | 3 | 2 | 3 |
| SL  | 7 | 2 | 2 | 3 | 3 | 2 | 3 | 0 | 3 | 3 | 4 | 2 | 3 | 3 | 8 | 2 | 2 | 4 | 4 | 0 |

To prove the proposed construction approach with LS heuristic is the best setting, the proposed approach of LS heuristic setting is applied to other problem instances that are available at http://tabu.diegm.uniud.it/ctt website such as comp07, comp08, comp09, comp10, comp11, comp12, comp13, comp14, comp15, comp16, comp17, comp18, comp19, comp20 and comp21. Table 9 shows the results of applying proposed construction approach with LS heuristic for the other problem instances. The approach can produce maximum population of feasible initial solution for most of the problem instances.

Table 9. Results of Feasible Initial Solution of Construction Approach with LS Heuristic for Other Instances

| Problem Instances | TOT  | MIN  | MAX  |
|-------------------|------|------|------|
| comp07            | 50   | 1043 | 1310 |
| comp08            | 50   | 790  | 929  |
| comp09            | 50   | 847  | 1064 |
| comp10            | 50   | 898  | 1074 |
| comp11            | 50   | 230  | 312  |
| comp12            | 50   | 1498 | 2044 |
| comp13            | 50   | 793  | 969  |
| comp14            | 50   | 745  | 903  |
| comp15            | 50   | 702  | 881  |
| comp16            | 50   | 949  | 1117 |
| comp17            | 48   | 902  | 1270 |
| comp18            | 50   | 583  | 773  |
| comp19            | 50   | 637  | 1225 |
| comp20            | 50   | 1042 | 1282 |
| comp21            | 50   | 928  | 1260 |

4. CONCLUSION

This paper portrays a construction approach that uses a combination of graph heuristics to construct a population of feasible initial timetables of curriculum based course timetabling problem. Results demonstrate that the construction approach with the use of largest degree followed by saturation degree setting is able to produce the maximum number of population instead of the use of single graph heuristics. The results of this study can contribute to the second phase of solving CBCTT problem that is the improvement stage, especially for population based metaheuristic methods.

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