Small-Signal Stability Modeling for MMC-Based DC Grids With Voltage Slope Control and Influence Analysis of Parameters

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ABSTRACT In the flexible DC grids, selections of slope coefficients in system level controls and designs of smoothing reactors have a crucial influence on the system stability. In order to obtain their optimal values, a comprehensive small-signal stability model with the DC voltage slope control and smoothing reactors is proposed in this paper. Firstly, the linear state-space model of the entire system based on the small-signal method is deduced according to the coupling equations between the inputs, the outputs, and state variables related to converter stations and the AC sides, controllers, and the DC grid with smoothing reactors. Meanwhile, the influences of the MMC bridge arm circulating current and the capacitor voltage fluctuation of the sub-module are considered in this model. Secondly, the impacts of control parameters, smoothing reactor parameters, and bridge arm inductances are analyzed on the system stability through the Lyapunov stability theory. Finally, the simulation of Zhangbei four-terminal DC grid project in China is established to testify the correctness of the presented small-signal model and the conclusions about the impact of parameters on the system stability. The proposed method will provide some theoretical guidance for the system design and the parameter selection in DC grid applications.

INDEX TERMS DC grids, modular multilevel converter, small-signal method, slope control, smoothing reactor.
MMC and DC voltage control were deduced, and a 16th-order interface with an external controller, AC system, and DC system. In [15], the internal dynamic characteristics of MMC and DC voltage control were deduced, and a 16th-order small-signal model of a single-terminal MMC was proposed. In [16], a small-signal impedance model of MMC including internal harmonic dynamics was presented for analyzing the resonance and stability of MMC-based systems. The research discussed above all focused on the stability of the single-terminal MMC system. A reduced-order model was proposed in [17] to solve the problem of high order in the MMC small-signal model, but it was only suitable for two terminal MMC-based HVDC system.

The MMC-MTDC systems have the characteristics of diverse converter types, changeable operation modes and complex control links, which makes the interaction law more complex between AC and DC system, among different control links, between DC grid and control systems. When the system fluctuates, the instability may occur. Therefore, it is necessary to study the interaction mechanism on stability analysis between AC and DC hybrid systems, so as to provide some theoretical guidance for the design and parameter selection of MMC-MTDC systems. In [18], a generic small-signal model of MMC based DC grid was established and a DC virtual impedance damping control was proposed to suppress the resonance and instability, which employed the averaged-value model of MMC. An accurate DC-side impedance modeling of MMC and a control strategy for improving the stability in MMC-based DC grid were presented in [19], which considered the coupling of internal multiple harmonics and the complete control system. These literatures all adopt the master-slave control strategy as system level controls in the stability modeling. As we know, the disadvantage of the master-slave control is that when the main converter station fails, the slave converter station can’t participate the controls of the DC voltage and power flow distribution, which leads to the instability of the whole system [20].

In addition, recent researches scarcely focus on the stability of DC grids with DC equipment, such as the current-limiting reactor, smoothing reactor. It is well known that the current-limiting reactor can assist the DC circuit breaker in removing DC faults [21]–[23], and the smoothing reactor can effectively suppress the harmonics of DC current, maintain the stability of DC side voltage, and reduce the impact of such large-capacity reactors increase the electrical distance between converter stations, which adversely affect the stability of the DC grid and the control of DC voltage.

Therefore, the main contributions of this article are as follows:

1) The interaction mechanism between converter stations using the DC voltage slope control strategy and DC gird with smoothing reactors is studied in this paper.

2) A comprehensive small-signal model of the MMC-based DC grid is proposed, which includes the internal dynamic behaviors of MMCs, converter stations, diverse controllers, and the DC grid with smoothing reactors.

3) On the base of the small-signal model, the influences of slope coefficient, PI parameter, smoothing reactor parameter and bridge arm inductance on the system stability are analyzed through Lyapunov stability theory and the root locus method. Thus, a theoretical basis of the system design and the parameter selection in DC grid applications is provided.

The rest of this article is organized as follows. A comprehensive small-signal stability model for MMC-based DC grids is proposed in Section II. The influences of control parameters, smoothing reactor parameters, and bridge arm inductances are analyzed on the system stability in Section III, obtaining their reasonable value ranges that would maintain the system stability. The correctness of the presented small-signal stability model is validated by a simulated four-terminal DC grid in Section IV. Conclusions are summarized in Section V.

II. SMALL-SIGNAL STABILITY MODELING FOR MMC-BASED DC GRIDS

A. SMALL-SIGNAL MODELING OF CONVERTER STATIONS AND AC SIDES

In this paper, the mathematical model of the converter station is obtained by considering the influence of the circulating current and the SM capacitor voltage fluctuation. Fig.1 shows the basic structure of the MMC station.

**FIGURE 1.** The basic structure of the MMC station.

In Fig.1, the SM adopts a semi-half-bridge structure. \(u_{pa}\) and \(u_{na}\) are the voltages of the upper and lower bridge arms, respectively. \(i_{pa}\) and \(i_{na}\) are the currents of the upper and lower bridge arm, respectively. \(R_{arm}\) and \(L_{arm}\) are the resistance and inductance of the bridge arm, respectively. \(R_f\) and \(L_f\) are the equivalent resistance and inductance for the AC side, respectively. \(i_{cir}\) is the circulating current of phase A bridge arm. \(\dot{U}_{dc}\) and \(\dot{I}_{dc}\) are the voltage and current of the DC side, respectively. \(u_k\) and \(i_k\) are the voltage and the current of the AC side, respectively. The subscript \(N\) is the number of SM in each bridge arm.
Take phase A as an example to establish the small-signal model between the converter station and the AC side. Considering the influences of the bridge arm circulating currents, the current $i_{pa}$ and $i_{na}$ are composed of the DC component, the fundamental frequency component and the double frequency circulating current component, ignoring the high-order circulating current components. The instantaneous value of the bridge arm current can be expressed as follows.

$$
\begin{align*}
    i_{pa} &= \frac{1}{3}I_{dc} - \frac{1}{2}I_{sa} \sin(\omega t + \beta_1) + I_{cira} \sin(2\omega t + \beta_2) \\
    i_{na} &= \frac{1}{3}I_{dc} + \frac{1}{2}I_{sa} \sin(\omega t + \beta_1) + I_{cira} \sin(2\omega t + \beta_2)
\end{align*}
$$

(1)

where $I_{sa}$ and $\beta_1$ are the amplitude and the phase angle of the fundamental frequency component, respectively. $I_{cira}$ and $\beta_2$ are the amplitude and the phase angle of the double frequency circulating current component, respectively.

Meanwhile, the SM capacitor voltage fluctuations are considered. The SM capacitor voltage $u_{ca}$ of the upper bridge arm at phase A is composed of the DC component $U_{c,dc}$, the fundamental frequency component $u_{ca,ac1}$ and the double frequency component $u_{ca,ac2}$, ignoring the components above triple frequency. The instantaneous value of the SM capacitor voltage can be expressed as follows.

$$
u_{ca} = U_{c,dc} + u_{ca,ac1} \sin(\omega t + \theta_1) + u_{ca,ac2} \sin(2\omega t + \theta_2)
$$

(2)

where $U_{ca,ac1}$ and $\theta_1$ are the amplitude and the phase angle of the fundamental frequency component, respectively. $U_{ca,ac2}$ and $\theta_2$ are the amplitude and the phase angle of the double frequency component, respectively.

If there are enough SMs of each bridge arm, the output voltage of the bridge arm can be considered continuous. Taking the upper bridge arm at phase A as an example, its average switching function model can be expressed as

$$
\begin{align*}
    S_p \cdot i_{pa} &= C \frac{du_{ca}}{dt} \\
    u_{pa} &= N \cdot S_p \cdot u_{ca}
\end{align*}
$$

(3)

where $C$ is the capacitance of the SM. $S_p$ is the average switching function of the upper bridge arm, namely

$$
S_p = \frac{1}{2} - \frac{1}{2}M \sin(\omega t + \alpha) + \frac{U_{cira}}{U_{dc}} \sin(2\omega t + \varphi)
$$

(4)

where $M$ and $\alpha$ are the modulation ratio and the phase angle of the fundamental frequency reference voltage, respectively. $U_{cira}$ and $\varphi$ are the amplitude and the phase angle of the voltage correction component in the circulating current suppressor, respectively.

Substituting Eq. (1) and Eq. (4) into Eq. (3), the dynamic equations of DC component, fundamental frequency component and double frequency component of the SM capacitor voltage are obtained in Eq. (5).

$$
\begin{align*}
    \frac{dU_{c,dc}}{dt} &= \frac{1}{6C}I_{dc} + \frac{U_{cira}I_{cira}}{2CU_{dc}} \cos(\varphi - \beta_2) \\
    &+ \frac{1}{8C}MI_{sa} \cos(\alpha - \beta_1) \\
    \frac{dU_{ca,ac1}}{dt} &= -\frac{1}{4C}I_{sa} \sin(\omega t + \beta_1) \\
    &- \frac{1}{4C}MI_{cira} \cos(\omega t + \beta_2 - \alpha) \\
    &- \frac{6C}{U_{dc}} \sin(\omega t + \alpha) - \frac{1}{2C}MI_{cira} \sin(2\omega t + \alpha + \beta_1) \\
    &+ \frac{1}{2C}I_{cira} \sin(2\omega t + \beta_2) + \frac{U_{cira}I_{dc}}{3CU_{dc}} \sin(2\omega t + \varphi)
\end{align*}
$$

(5)

Combined with the three-phase expressions of Eq. (5), the state equations of the SM capacitor voltage represented by d-q component are obtained in Eq. (6) after d-q transforms of positive-sequence fundamental frequency and negative-sequence double frequency, respectively.

$$
\begin{align*}
    \frac{dU_{c,dc}}{dt} &= \frac{I_{dc}}{6C} + \frac{U_{c1d}I_{sd}}{4CU_{dc}} + \frac{U_{c1d}I_{sq}}{4CU_{dc}} + \frac{U_{c1q}I_{cird}}{2CU_{dc}} \\
    \frac{dU_{c,ac1}}{dt} &= -\omega U_{c,ql} - \frac{U_{c1d}I_{ld}}{3CU_{dc}} - \frac{I_{sd}}{4C} - \frac{U_{c1d}I_{ld}}{4CU_{dc}} \\
    \frac{dU_{c,ac2}}{dt} &= \omega U_{c,ql} - \frac{U_{c1d}I_{ld}}{3CU_{dc}} - \frac{I_{sd}}{4C} - \frac{U_{c1d}I_{ld}}{4CU_{dc}} - \frac{I_{sq}}{2CU_{dc}} \\
    \frac{dU_{c,d1}}{dt} &= -\omega U_{c,q2} - \frac{U_{cird}I_{ld}}{3CU_{dc}} + \frac{U_{c1d}I_{ld}}{4CU_{dc}} - \frac{U_{c1q}I_{sq}}{4CU_{dc}} \\
    \frac{dU_{c,d2}}{dt} &= 2\omega U_{c,d2} + \frac{U_{cird}I_{ld}}{3CU_{dc}} - \frac{U_{c1d}I_{ld}}{4CU_{dc}} - \frac{U_{c1q}I_{sq}}{4CU_{dc}} \\
    \frac{dU_{c,q2}}{dt} &= 2\omega U_{c,q2} + \frac{U_{cird}I_{ld}}{3CU_{dc}} - \frac{U_{c1d}I_{ld}}{4CU_{dc}} - \frac{U_{c1q}I_{sq}}{4CU_{dc}}
\end{align*}
$$

(6)

where $U_{c1d}$ and $U_{c1q}$ represent the d-q components of the fundamental frequency component $U_{ca,ac1}$, respectively. $U_{c2d}$ and $U_{c2q}$ represent the d-q components of the double frequency component $U_{ca,ac2}$, respectively. $U_{sd}$, $U_{sq}$, $I_{sd}$, $I_{sq}$ represent the d-q components of the voltage and the current at the AC side, respectively. $I_{cird}$ and $I_{cirq}$ represent the d-q components of the double-frequency circulating current. $U_{cird}$ and $U_{cirq}$ represent the d-q components of the double-frequency modulation voltage output by the circulating current suppressor. $U_{c1d}$ and $U_{c1q}$ are the d-q components of the three-phase fundamental frequency reference voltages, namely

$$
\begin{align*}
    U_{c1d} &= MU_{dc} \sin \alpha/2 \\
    U_{c1q} &= MU_{dc} \cos \alpha/2
\end{align*}
$$
Substituting Eq. (2) and Eq. (4) into Eq. (3), the DC component \(U_{pa, dc}\), the fundamental frequency component \(u_{pa, ac1}\) and the double frequency component \(u_{pa, ac2}\) of the upper bridge arm voltage are obtained in Eq. (7), ignoring the components above triple frequency.

\[
\begin{align*}
U_{pa, dc} &= \frac{1}{2} NU_{c, dc} - \frac{1}{4} NMU_{ca, ac1} \cos (\alpha - \theta_1) \\
U_{cira} &= -\frac{1}{2} NU_{c, ac2} \cos (\phi - \theta_2) \\
u_{pa, ac1} &= -\frac{1}{2} NU_{c, dc} \sin (\omega t + \phi) + \frac{1}{2} NU_{ca, ac1} \sin (\omega t + \theta_1) \\
u_{cira} &= \frac{1}{2} NU_{c, ac1} \cos (\omega t + \phi - \theta_2) \\
u_{pa, ac2} &= -\frac{1}{4} NU_{c, ac2} \cos (\omega t + \theta_2 - \alpha) \\
u_{cira} &= \frac{1}{2} NU_{c, ac1} \cos (2\omega t + \phi) + \frac{1}{2} NU_{ca, ac2} \sin (2\omega t + \theta_2) \\
+ \frac{1}{4} NMU_{ca, ac1} \cos (2\omega t + \theta_1 + \alpha)
\end{align*}
\]

(7)

According to the KVL, the voltage relations to the DC side and the AC side of the converter in Fig. 1 can be expressed as follows.

\[
\begin{align*}
U_{dc} &= 2U_{pa, dc} + \frac{2}{3} R_{arm} I_{dc} + \frac{2}{3} L_{arm} \frac{dI_{dc}}{dt} \\
u_{sa} &= -u_{pa, c1} + L_{eq} \frac{di_{sa}}{dt} + R_{eq} i_{sa} \\
2u_{pa, c2} + 2L_{arm} \frac{dc_{cira}}{dt} + 2R_{arm} i_{cira} &= 0
\end{align*}
\]

(8)

where \(L_{eq} = L_t + L_{arm}/2\), \(R_{eq} = R_t + R_{arm}/2\).

Substituting Eq. (7) into Eq. (8), the state equations of the DC side current, the AC side current and the circulating current related to phase A can be expressed in Eq. (9).

\[
\begin{align*}
d\frac{d}{dt} &= \frac{3U_{dc}}{2L_{arm}} - \frac{R_{arm} I_{dc}}{L_{arm}} - \frac{3NU_{c, dc}}{2L_{arm}} \\
&+ \frac{3NU_{c, ac1} \cos (\alpha - \theta_1)}{4L_{arm}} \\
&+ \frac{2RU_{dc}}{L_{eq}} - \frac{R_{eq} i_{sa}}{L_{eq}} - \frac{NU_{c, dc} \cos (\omega t + \phi - \theta_2)}{2L_{eq}} \\
&- \frac{NU_{ca, ac2} \cos (\omega t + \phi)}{2L_{eq}} \\
&- \frac{NU_{ca, ac1} \cos (\omega t + \theta_2 - \alpha)}{2L_{eq}} \\
&- \frac{4RU_{dc}}{2L_{arm}} - \frac{R_{arm} i_{cira}}{L_{arm}} - \frac{NU_{c, dc} \sin (2\omega t + \phi)}{L_{arm} U_{dc}} \\
&- \frac{NU_{ca, ac2} \sin (2\omega t + \theta_2)}{2L_{arm}} \\
&- \frac{NU_{ca, ac1} \cos (2\omega t + \theta_1 + \alpha)}{2L_{arm}}
\end{align*}
\]

(9)

Combined with the three-phase expressions of Eq. (9), the station equations of the DC side current, the AC side current and the circulating current represented by d-q component are obtained after d-q transforms of positive-sequence fundamental frequency and negative-sequence double frequency, respectively.

\[
\begin{align*}
\frac{dI_{dc}}{dt} &= -\frac{3NU_{c, dc}}{2L_{arm}} + \frac{3NU_{c, dc}}{2L_{arm} U_{dc}} + \frac{3NU_{c, dc}}{2L_{arm} U_{dc}} \\
&- 3RU_{dc} I_{dc} + \frac{3U_{dc}}{2L_{arm}} + \frac{3U_{dc}}{2L_{arm} U_{dc}} \\
\frac{dI_{arm}}{dt} &= -\frac{3RU_{arm} I_{arm}}{2L_{eq}} + \frac{3U_{arm} I_{arm}}{2L_{eq}} + \frac{3U_{arm} I_{arm}}{2L_{eq}} \\
\frac{dI_{eq}}{dt} &= -\frac{3RU_{arm} I_{eq}}{2L_{arm}} + \frac{3U_{arm} I_{eq}}{2L_{arm}} + \frac{3U_{arm} I_{eq}}{2L_{arm}} \\
\end{align*}
\]

(10)

Combined with Eq. (6) and Eq. (10), the 10\textsuperscript{th} order small-signal model of the single-ended MMC station after linearization at a certain steady-state operation point is obtained in Eq. (11).

\[
\begin{align*}
\Delta \dot{x} &= A \Delta x + B_1 \Delta u \\
\Delta y &= C_\Delta \Delta x + D_1 \Delta u
\end{align*}
\]

(11)

where the state variable matrix and the input variable matrix are shown, namely

\[
\Delta x = [\Delta U_{c, dc} \Delta U_{c, 1d} \Delta U_{c, 1q} \Delta U_{c, 2d} \Delta U_{c, 2q} \Delta I_{dc} \Delta I_{id} \Delta I_{sq} \Delta I_{cird} \Delta I_{cirq}]^T
\]

\[
\Delta y = [\Delta U_{c, 1d} \Delta U_{c, 1q} \Delta I_{cird} \Delta I_{cirq} \Delta U_{id} \Delta U_{sq} \Delta U_{id} \Delta U_{sq} \Delta U_{dc} \Delta I_{dc}]^T
\]

where the input variables \(\Delta U_{id}\) and \(\Delta U_{sq}\) provide an interface to the AC system. The input variable \(\Delta U_{dc}\) provides an interface to the DC side. The input variable \(\Delta \omega\) provide an interface to the PLL controller. The input variables \(\Delta U_{c, 1d}\) and \(\Delta U_{c, 1q}\) provide an interface to the main controller. The input variables \(\Delta U_{c, 1d}\) and \(\Delta U_{c, 1q}\) provide an interface to the circulating current suppressor.
B. SMALL-SIGNAL MODELING OF CONTROL SYSTEMS

1) MODELING OF THE DC VOLTAGE SLOPE CONTROLLER

In the MMC-MTDC transmission system, the DC voltage slope control is increasingly being used to realize DC voltage coordinated control among multiple converter stations. It is superior to the master-slave control, because there is no need to switch the working modes of MMC, and no communication between stations either [26]. However, inappropriate slope coefficients will have a certain influence on the system stability. In this paper, a small-signal model based on the DC voltage slope control is proposed for the slope coefficient setting. Fig. 2 shows the structure of the main controller based on DC voltage slope control.

\[
\begin{align*}
\mathbf{1} & \mathbf{1} \\
\mathbf{x} & = \mathbf{A} \mathbf{x} + \mathbf{B} \mathbf{u} + \mathbf{C} \mathbf{d} \\
\mathbf{y} & = \mathbf{D} \mathbf{x} + \mathbf{E} \mathbf{u} + \mathbf{F} \mathbf{d}
\end{align*}
\]

where \( P_{\text{ref}} \) and \( P_m \) are the reference and the measured values of active power, respectively. \( Q_{\text{ref}} \) and \( Q_m \) are the reference and the measured values of reactive power, respectively. \( U_{\text{dcref}} \) is the reference value of DC voltage. \( I_{\text{dref}} \) and \( I_{\text{qref}} \) are the reference values of the inner loop currents, respectively.

At this time, the influences of coefficient \( k \) and the active power deviation are considered to the outer loop controller. For the two integral elements of the outer loop in Fig. 2, two state variables are introduced, respectively.

\[
\begin{align*}
x_1 & = \int (U_{\text{dcref}} - U_{\text{dc}}) \, dr = \frac{dx_1}{dr} = U_{\text{dcref}}' - U_{\text{dc}} \\
x_2 & = \int (Q_{\text{ref}} - Q_m) \, dr = \frac{dx_2}{dr} = Q_{\text{ref}} - Q_m
\end{align*}
\]

where \( U_{\text{dcref}}' \) is the revised value of \( U_{\text{dcref}} \) after the slope control, namely

\[
U_{\text{dcref}}' = U_{\text{dcref}} + k(P_{\text{ref}} - P_m)
\]

The active power \( P_m \) and the reactive power \( Q_m \) can be expressed as follows.

\[
\begin{align*}
P_m & = \frac{3}{2} (U_{\text{sd}}I_{\text{sd}} + U_{\text{sq}}I_{\text{sq}}) \\
Q_m & = \frac{3}{2} (U_{\text{sd}}I_{\text{sq}} - U_{\text{sq}}I_{\text{sd}})
\end{align*}
\]

2) MODELING OF THE CIRCULATING CURRENT SUPPRESSOR

As the special structure and the modulation mode of MMC lead to the inconsistency between the voltages of the upper and lower bridge arms, and form the internal circulations which cause the distortion of the bridge arm currents. The circulating current suppressor is introduced to weaken the double frequency negative-sequence circulating current and reduce the loss of the converter. The structure of the circulating current suppressor is shown in Fig. 3.

\[
\begin{align*}
I_{\text{dircref}} & = k_{pp}(U_{\text{dcref}}' - U_{\text{dc}}) + k_{ip}x_1 \\
I_{\text{qircref}} & = k_{pq}(Q_{\text{ref}} - Q_m) + k_{iq}x_2
\end{align*}
\]

where \( k_{pp} \) and \( k_{pq} \) are the proportional gains of the outer loop controller. \( k_{ip} \) and \( k_{iq} \) are the integral gains of the outer loop controller.

For the two integral elements of the inner loop in Fig. 2, two state variables are introduced, respectively.

\[
\begin{align*}
\frac{dx_3}{dr} & = I_{\text{dref}} - I_{\text{sd}} \\
\frac{dx_4}{dr} & = I_{\text{qref}} - I_{\text{sq}}
\end{align*}
\]

The outputs of the main controller (namely the inputs of the MMC model) in Fig. 2 can be expressed as

\[
\begin{align*}
U_{\text{c1d}} & = U_{\text{sd}} - \omega L_{\text{eq}}I_{\text{sq}} - [k_{p1}(I_{\text{dref}} - I_{\text{sd}}) + k_{i1}x_3] \\
U_{\text{c1q}} & = U_{\text{sq}} + \omega L_{\text{eq}}I_{\text{sd}} - [k_{p1}(I_{\text{qref}} - I_{\text{sq}}) + k_{i1}x_4]
\end{align*}
\]

where \( k_{p1} \) and \( k_{i1} \) are the proportional and the integral gain of the inner loop controller, respectively.
For the two integral elements of PI controls in Fig. 3, two state variables are introduced, respectively.

\[
\begin{align*}
\frac{df_1}{dt} &= I_{\text{circ ref}} - I_{\text{circ}} \\
\frac{df_2}{dt} &= I_{\text{circ ref}} - I_{\text{circ}}
\end{align*}
\] (17)

The outputs of the circulating current suppressor (namely the inputs of the MMC model) can be expressed as follows.

\[
\begin{align*}
U_{\text{circ}1} &= 2\omega L_{\text{arm}} I_{\text{circ1}} + k_p (I_{\text{circ ref}} - I_{\text{circ}}) + k_i f_1 \\
U_{\text{circ}2} &= -2\omega L_{\text{arm}} I_{\text{circ2}} + k_p (I_{\text{circ ref}} - I_{\text{circ}}) + k_i f_2
\end{align*}
\] (18)

where \( k_p \) and \( k_i \) are the proportional and integral gain of the circulating current suppressor, respectively.

The state space model of the converter station control system is obtained according to Eq. (12) ~ Eq. (18), and its small-signal model after linearization is shown as follows.

\[
\begin{align*}
\dot{\Delta x}_c &= A_c \Delta x_c + B_c \Delta u_c \\
\Delta y_c &= C_c \Delta x_c + D_c \Delta u_c
\end{align*}
\] (19)

where;

\[
\begin{align*}
\Delta x_c &= [\Delta f_1, \Delta f_2, \Delta x_1, \Delta x_2, \Delta x_3, \Delta x_4]^T; \\
\Delta u_c &= [\Delta I_{\text{sd}}, \Delta I_{\text{sq}}, \Delta I_{\text{cird}}, \Delta U_{\text{sd}}, \Delta U_{\text{sq}}, \\
&\quad \Delta U_{dc}, \Delta U_{\text{ref}}, \Delta U_{\text{dc ref}}]^T; \\
\Delta y_c &= [\Delta U_{1,1d}, \Delta U_{1,1q}, \Delta U_{\text{cird}}, \Delta U_{\text{cirq}}]^T.
\end{align*}
\]

Thus, the small-signal model of the single-ended MMC station is obtained by combining Eq. (11) and Eq. (19) as follows.

\[
\begin{align*}
\dot{\Delta x}_m &= A_m \Delta x_m + B_m \Delta u_m
\end{align*}
\] (20)

where

\[
\Delta x_m = [\Delta u_1, \Delta u_2]^T, \quad \Delta u_m = [\Delta u_{1,1}, \Delta u_{2,2}]^T,
\]

\[
A_m = \begin{bmatrix}
A_c + B_c D_c E & B_c C_c \\
B_c E & A_c
\end{bmatrix}, \quad B_m = \begin{bmatrix}
B_{c \text{ref}} \quad B_{c \text{ref}} \\
0 & B_{c \text{ref}}
\end{bmatrix},
\]

\[
E = \begin{bmatrix}
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
\end{bmatrix}.
\]

\( \Delta u_{1,1} \) is the first four variables of \( \Delta u_{1} \), \( \Delta u_{2,2} \) is the last six variables of \( \Delta u_{2} \). \( B_{c,1} \) is the first four columns of \( B_{c} \), and \( B_{c,2} \) is the last four columns of \( B_{c} \). \( B_{c,1} \) is the first four columns of \( B_{c} \). \( B_{c,2} \) is the last six columns of \( B_{c} \). \( D_{c,1} \) is the first four columns of \( D_{c} \), and \( D_{c,2} \) is the last six columns of \( D_{c} \).

C. SMALL-SIGNAL MODELING OF DC TRANSMISSION LINES WITH SMOOTHING REACTORS

Fig. 4 is the single-pole diagram of Zhangbei four-terminal flexible DC grid with smoothing reactors, in which Kangbao station and Zhangbei station are sending terminals, Fengning station is a regulating terminal and Beijing station is a receiving terminal. In order to determine the optimal value of the smoothing reactor taking into account both the harmonic current suppression and the system stability, a small-signal model of DC lines with smoothing reactors is built.

In Fig. 4, \( U_{dc1} \) and \( I_{dc} \) are the voltage and the current at the DC side of the \( j \)-th MMC station, \( j = 1, 2, 3, 4 \). \( L_{s12}, L_{s13}, L_{s24} \) and \( L_{s34} \) are the smoothing reactors on the DC lines. For simplifying analysis, the \( \pi \)-type model expressed by lumped parameters is used to simulate the DC lines. Considering that the smoothing reactor has no DC voltage drop in the steady state, the grounded capacitances of the two lines connecting to the same MMC station are combined to get the simplified form of state-space equations. For example, the state-space equations about the current \( I_{13} \) and the voltage \( U_{dc1} \) are expressed as follows, according to KCL and KVL.

\[
\begin{align*}
\frac{df_{13}}{dt} &= \frac{1}{2L_{s13} + L_{f}} (-I_{13} R_{13} + U_{dc1} - U_{dc3}) \\
\frac{dU_{dc1}}{dt} &= \frac{1}{C_{12} + C_{13}} (U_{dc1} - I_{12} - I_{13})
\end{align*}
\]

Then, a small-signal model of four-terminal equivalent DC power grid can be deduced in Eq. (21).

\[
\begin{align*}
\Delta x_g &= A_g \Delta x_g + B_g \Delta u_g \\
\Delta y_g &= C_g \Delta x_g + D_g \Delta u_g
\end{align*}
\] (21)

where \( \Delta x_g = [\Delta I_L, \Delta U_{dc}]^T \) is the state variable \( \Delta I_L, \Delta y_g, \Delta u_g, A_g, B_g, D_g, F_1 - F_4 \), as shown at the bottom of the next page.

Finally, a comprehensive small-signal stability model for MMC-based DC grids is established by combining Eq. (20) and Eq. (21), considering the internal dynamic characteristics of the MMC, the DC voltage slope control, the function of the circulating current suppressor and the smoothing reactors. The block form of the model is shown in Eq. (22).
where the state matrix is denoted as \( \mathbf{A} \), and its order is 72 \( \times \) 72. On the base of the small-signal model, the influences of slope coefficient, PI control parameter, smoothing reactor parameter, and bridge arm inductance on the system stability are analyzed using Lyapunov stability theory and the root locus method.

### III. STABILITY ANALYSIS

The Zhangbei Project in Fig. 4 is used to analyze the influences of various parameters, in which the DC voltage slope control is adopted at the Fengning station and the Beijing station, and the constant active power control is adopted at other two stations. Table 1 shows the main parameters of each converter station. Table 2 shows the main parameters of DC transmission lines.

#### A. INFLUENCE ANALYSIS OF CONTROL PARAMETERS IN DC VOLTAGE SLOPE CONTROLLER

Taking Fengning station as an example, the influences of the DC voltage slope coefficient and the outer loop PI control parameters on system stability are analyzed.
1) THE DC VOLTAGE SLOPE COEFFICIENT
Improper values of slope coefficients will directly affect the voltage compensated values required by each converter stations to meet the system stability, resulting in the system instability. Suppose that the slope coefficient $k$ in Fig. 2 increases from 0.1 to 1 at step 0.01, and other control parameters remain unchanged. Fig. 5 shows the root locus of dominant poles when the slope $k$ changes.

![FIGURE 5. Root locus of dominant poles when the slope $k$ changes.](image)

In Fig. 5, as the slope coefficient $k$ increases, the root locus of dominant poles moves from the left-half to the right-half on the complex plane. When $k = 0.25$, the root locus crosses the imaginary axis, and the system loses stability. Therefore, the value of the slope parameter $k$ must be less than 0.25 if the system keeps stable in this example.

2) THE OUTER LOOP PI CONTROL PARAMETERS
In Fig. 2, suppose that the outer loop proportional gain $k_{pp}$ increases from 10 to 20 at step 0.1, the integral gain $k_{ip}$ increases from 0.1 to 10 at step 0.1, respectively. Other parameters remain unchanged. Fig. 6 shows the root locus diagrams of their dominant poles when they change separately.

![FIGURE 6. Root locus of PI control parameters at Fengning station.](image)

(a) Proportional gain $k_{pp}$ and (b) integral gain $k_{ip}$.

In Fig. 6(a), as the proportional gain $k_{pp}$ increases, its root locus of the modes related to the double frequency circulating current moves on the left-half plane and is gradually away from the imaginary axis. This shows that the corresponding modes of the double frequency circulating current enhance the system stability and weaken the suppression effect on the circulating current.

In Fig. 6(b), as the integral gain $k_{ip}$ increases, its root locus of the modes related to the double frequency circulating current still moves on the left-half plane and gradually approaches the imaginary axis. The results show that the corresponding modes of the double frequency circulating current only weaken the system stability and enhance the suppression effect on the circulating current.

B. INFLUENCE ANALYSIS OF CIRCULATION SUPPRESSOR CONTROL PARAMETERS
Take Kangbao Station as an example to analyze the influence of control parameters in the circulating current suppressor on the stability of the system. In Fig. 3, suppose that the proportional gain $k_{p2}$ increases from 10 to 15 at step 0.1, and the integral gain $k_{i2}$ increases from 5 to 10 at step 0.1, respectively. Other parameters remain unchanged. Fig. 7 shows the root locus of the modes related to the double frequency circulating current when they change separately.

In Fig. 7(a), as the proportional gain $k_{p2}$ increases, its root locus of the modes related to the double frequency circulating current moves on the left-half plane and is gradually away from the imaginary axis. This shows that the corresponding modes of the double frequency circulating current enhance the system stability and weaken the suppression effect on the circulating current.

In Fig. 7(b), as the integral gain $k_{i2}$ increases, its root locus of the modes related to the double frequency circulating current still moves on the left-half plane and gradually approaches the imaginary axis. The results show that the corresponding modes of the double frequency circulating current only weaken the system stability and enhance the suppression effect on the circulating current.
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FIGURE 7. Root locus of the double-frequency circulating current at Kangbao station. (a) Proportional gain $k_{p2}$ and (b) integral gain $k_{i2}$.

C. INFLUENCE ANALYSIS OF SMOOTHING REACTOR PARAMETER

The selection of the smoothing reactor parameter should not only take into account the effect of the DC current harmonic suppression, but also ensure the system stability. Suppose that smoothing reactor parameters $L_s$ in Fig. 4 gradually increases from 0.1H to 0.7H at step 0.01H. Fig. 8 shows the root locus diagram of dominant poles when $L_s$ changes.

FIGURE 8. Root locus of dominant pole when $L_s$ changes.

As seen in Fig. 8, the root locus of dominant pole moves from the left-half to the right-half on the complex plane. When $L_s = 0.48$H, the root locus crosses the imaginary axis, and the system loses the stability. Thus, the value of the smoothing reactor $L_s$ must be less than 0.48H if the system keeps stable in this example.

D. INFLUENCE ANALYSIS OF MMC BRIDGE ARM INDUCTANCE

The upper and lower bridge arm reactors of MMC are used to suppress the interphase circulation caused by the bridge arms' voltage imbalance, and inappropriate parameters will also affect the stability of the system. Taking the Kangbao station as an example, the influence of MMC bridge arm inductance on the system stability is analyzed. Set that the inductance $L_{arm}$ of the three-phase bridge arms in Fig. 1 increases from 0.05H to 0.5H at 0.01H step. Fig. 9 shows the root locus of dominant pole when $L_{arm}$ changes.

FIGURE 9. Root locus of dominant poles when $L_{arm}$ changes.

In Fig. 9, as the inductance $L_{arm}$ increases, the root locus of dominant poles also moves from the left-half to the right-half on the complex plane. When the inductance $L_{arm}$ is more than 0.39H, the system loses stability. Hence, the selection of the MMC bridge arm inductance $L_{arm}$ must be less than 0.39H for the system stability in this example.

IV. SIMULATION

To testify the correctness of the presented small-signal model and the conclusions about the impact of various parameters on the system stability, the simulation of the Zhangbei project in China is established via PSCAD/EMTDC platform. The simulation time is 5s. Under the initial conditions, the Kangbao station sends 1500MW, the Zhangbei station sends 3000MW, the Fengning station receives 1500MW and the Beijing station receives 3000MW.

A. SIMULATION OF SLOPE COEFFICIENT IN DC VOLTAGE SLOPE CONTROLLER

Unreasonable selection of the slope coefficient $k$ will affect the stability of the system. In A of Section III, the conclusion of the stability analysis is given, that is, the slope parameter $k$ must be less than 0.25 if the system keeps stable. Taking Fengning station as an example, the slope coefficient $k$ is set as 0.1 and 0.3, respectively. When the power of Fengning station drops from 1500MW to 1200MW in 3s, the power waveforms with different $k$ values at Fengning station are shown in Fig. 10.

As seen in Fig. 10(a), the active power waveform at Fengning station can quickly track a given value 1200WM after 3s, the overshoot of waveform is very small and the transient time is very short, when the slope coefficient $k$ is set as 0.1. In this case, the system still remains stable. In Fig. 10(b), the overshoot of waveform reaches 200MW, the active power receiving has deviated from the given value 1200MW and always oscillates after 3s, when the slope coefficient $k$ is set as...
0.3. In this case, the system is unstable so that it cannot reach a new stable state. This simulation proves that the conclusion about the slope coefficient $k$ in $A$ of Section III is correct.

### B. SIMULATION OF OUTER LOOP PROPORTIONAL GAIN IN DC VOLTAGE SLOPE CONTROLLER

Improper selection of the outer loop proportional gain in the DC voltage slope controller will also affect the stability of the system. In $A$ of Section III, the conclusion of the stability analysis is given, that is, the value of the proportional gain $k_{pp}$ must be less than 17.8 if the system keeps stable. Taking Fengning station as an example, the proportional gain $k_{pp}$ in the DC voltage slope controller is set as 10 and 18, respectively. When the receiving power at Fengning station drops from 1500MW to 1200MW in 3s, the active power waveforms with different $k_{pp}$ value at Fengning station are shown in Fig.11.

As seen in Fig. 11(a), the power waveform can quickly track a given value 1200MW after 3s, the overshoot of waveform is very small and the transient time is very short, when the proportional gain $k_{pp}$ is set as 10. In this case, the system still keeps stable. In Fig.11(b), the overshoot of waveform is more than 300MW, and the waveform oscillates seriously after 3s, when the proportional gain $k_{pp}$ is set as 18. In this case, the system losses its stability. This simulation proves that the conclusion about the outer loop proportional gain $k_{pp}$ of the DC voltage slope controller in $A$ of Section III is correct.

### C. SIMULATION OF PI CONTROL PARAMETERS IN CIRCULATION CURRENT SUPPRESSOR

In order to prove that control parameters in the circulating current suppressor have the effect of restraining the circulating current and have litter effect on the system stability, take Kangbao station as the tested object. The circulating current suppressor doesn’t run at the initial time. When the system runs to 2s, put the circulating current suppressor into operation. When the system runs to 3s, change control parameters of the suppressor. The circulating current waveforms in the three cases are compared.

1) SIMULATION OF PROPORTIONAL GAIN IN THE CIRCULATION CURRENT SUPPRESSOR

Suppose that the initial value of the proportional gain $k_{p2}$ is set to 10. When the system runs to 3s, the proportional gain $k_{p2}$ is set as 30, and other parameters remain unchanged. Fig.12 shows the double frequency circulating current waveform in the three cases at the Kangbao station.

In Fig.12, the circulating current is changed between $[-1.5, 1.5]$ kA before 2s, and its amplitude is relatively large. The circulating current suppressor runs after 2s, the
circulating current decreases, and this shows that the circulating current suppressor can effectively suppress the circulating current. Moreover, when the proportional gain $k_{p2}$ is increased from 10 to 30 at 3s, the circulating current is changed from zero to $[-0.5, 0.5]$ kA, and the circulating current suppression effect is weakened.

2) SIMULATION OF INTEGRAL GAIN IN THE CIRCULATION CURRENT SUPPRESSOR
When the system runs to 2s, the circulating current suppressor puts into operation, and the initial value of its integral gain $k_{i2}$ is set as 5. When the system runs to 3s, the integral gain $k_{i2}$ is increased to 10, and other parameters remain unchanged. Fig. 13 shows the double frequency circulating current waveform in the three cases at the Kangbao station.

In Fig.13, the circulating current suppressor runs after 2s, the circulating current decreases, and this shows that the circulating current suppressor can effectively suppress the circulating current. Moreover, when the proportional gain $k_{i2}$ is increased from 5 to 10 at 3s, the circulating current is changed from $[-0.6, 0.6]$ to $[-0.1, 0.1]$ kA, and the circulating current suppression effect is enhanced.

The above verifies the correctness of the conclusions about control parameters of the circulating current suppressor in B of Sections III.

D. SIMULATION OF SMOOTHING REACTOR PARAMETERS
Unreasonable selection of smoothing reactor parameter $L_s$ will affect the stability of the system. In C of Section III, the conclusion of the stability analysis is given, that is, the parameter $L_s$ must be less than 0.48H if the system remains stable. Suppose that the smoothing reactor parameters $L_s$ are set as 0.2H and 0.5H, respectively. When the system runs to 3s, the received power at Beijing station step from 3000WM to 3300MW. The received power waveforms at Beijing station under different smoothing reactors are shown in Fig. 14.

As shown in Fig. 14(a), the received power at Beijing station can accurately track a given value after 3s and the system still remains stable, when the smoothing reactor parameters $L_s$ are 0.2H. In Fig. 14(b), when the parameters $L_s$ are 0.5H, the received power fluctuates greatly after 3s, resulting in the system instability. The simulation verifies the correctness of the conclusion about smoothing reactor parameters in C of Section III.

V. CONCLUSION
By studying the interaction mechanism between converter stations using the DC voltage slope control and DC grids with smoothing reactors, this paper develops a comprehensive small-signal stability model of the MMC-based DC grid, which also includes the internal dynamic behaviors of MMCs and the circulating current suppressor. The proposed method provides some theoretical guidance for the system design and the parameter selection in DC grid applications as follows.

1) The slope coefficient has a great influence on the system stability and power balance. When the slope coefficient exceeds a certain threshold, the active power fluctuations at the converter station increase significantly, resulting in the system instability.

2) The outer loop proportional gain of the DC voltage slope controller has a certain influence on the system stability. If the proportional gain exceeds a threshold value, the system will be unstable.

3) The values of the smoothing reactor and MMC bridge arm reactor will also affect the system stability. The system will lose stable when these two parameters exceed their respective thresholds.

4) The PI control parameters of the circulating current suppressor doesn’t only affect the system stability, but also have an impact on the suppression effect of the double frequency circulating current.
In this paper, the balanced condition is only considered. In fact, the unbalance condition is a more practical event. In the case of unbalance condition, the AC current on the MMC valve side will have a negative-sequence component of fundamental frequency, and the bridge arm currents of the MMC converter will appear the zero-sequence double-frequency circulating currents [27]. The stability analysis of MMC-based DC grids under unbalanced AC system is the future work.

APPENDIX
The coefficient matrices $A_s$ and $B_s$, as shown at the top of the page, of Eq. (11) are shown as follows, respectively.

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