Hierarchical Object-to-Zone Graph for Object Navigation

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Abstract

The goal of object navigation is to reach the expected objects according to visual information in the unseen environments. Previous works usually implement deep models to train an agent to predict actions in real-time. However, in the unseen environment, when the target object is not in egocentric view, the agent may not be able to make wise decisions due to the lack of guidance. In this paper, we propose a hierarchical object-to-zone (HOZ) graph to guide the agent in a coarse-to-fine manner, and an online-learning mechanism is also proposed to update HOZ according to the real-time observation in new environments. In particular, the HOZ graph is composed of scene nodes, zone nodes and object nodes. With the pre-learned HOZ graph, the real-time observation and the target goal, the agent can constantly plan an optimal path from zone to zone. In the estimated path, the next potential zone is regarded as sub-goal, which is also fed into the deep reinforcement learning model for action prediction. Our methods are evaluated on the AI2-Thor simulator. In addition to widely used evaluation metrics SR and SPL, we also propose a new evaluation metric of SAE that focuses on the effective action rate. Experimental results demonstrate the effectiveness and efficiency of our proposed method. The code is available at https://github.com/sx-zhang/HOZ.git.

1. Introduction

Visual navigation task requires the agent to reach a specified goal. Conventional methods usually require spatial layout information, such as maps of the environments, which can be easily obtained in seen environments while unavailable in unseen environments. Therefore, how to efficiently navigate to the target in unseen environments is typically challenging.

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With the visual input of egocentric observation, previous works [31, 29, 30] learn a deep reinforcement learning policy by maximizing the reward. The key challenge in those works is the generalization to unseen environments [40], especially when the target is not in the sight. Therefore, more recent works [43, 11] attempt to embed prior knowledge, such as object graph and relation graph, to improve the navigation model’s generalization ability. In particular, Yang et al. [43] construct an object-to-object graph, which provides correlated objects as auxiliary information to locate the target object. Their object graph is too general to fit into specific environments. Additionally, Du et al. [11] propose to learn object relation graph, which fits the testing environments better than the general object graph. The above approaches focus on constructing object-oriented graph to provide some clues to the navigation when the target is not
in the view. However, since object relations and spatial layout are usually inconsistent in different environments, the generalization ability of the above methods are still limited.

Motivated by enhancing the generalization ability of the navigation model, we carry out this study from two aspects: 1) learning an adaptive spatial knowledge representation that is applicable to various environments; 2) adapting the learned knowledge to guide navigation in the unseen environments. Besides, regions in larger area are considered in our knowledge, which are denoted as zones. Compared with objects, larger zones are more likely to be observed by agent. Thus our core idea for navigation guidance is zone.

In this paper we propose the hierarchical object-to-zone (HOZ) graph to capture the prior knowledge of scene layout for object navigation (see Figure 1). During training, we construct a general HOZ graph from all scenes, as rooms in the same scene category have same spatial structures. Each scene node corresponds to a scene-wise HOZ graph, whose zone nodes are obtained by matching and merging the room-wise HOZ graphs. For each room-wise HOZ graph, each zone node represents a group of relevant objects and each zone edge models the adjacent probability of two zones. Then we train a zone-to-action LSTM policy via deep reinforcement learning in the photo-realistic simulator AI2-Thor [21]. For each episode, the pre-learned HOZ graph helps to plan an optimal path from current zone to target zone, thus deducing the next potential zone on the path as a sub-goal. The sub-goal is embedded with graph convolutional network (GCN) to predict actions. Considering that different environments have diverse zone layouts, we also propose an online-learning mechanism to update the general learned HOZ graph according to current unseen environment. In this way, the initial HOZ graph will evolve towards current environment’s specific layout and help agent to navigate successfully. Note that the update only holds for an episode and each episode starts from the initial HOZ graph. In addition to widely used evaluation metrics Success Rate (SR) and Success weighted by Path Length (SPL), we also propose a new evaluation metric of Success weighted by Action Efficiency (SAE) that considers the efficiency of the navigation action into SR. Our experiments show that the HOZ graph outperforms the baseline by a large margin. In summary, our contributions are as follows:

- We propose to learn the hierarchical object-to-zone (HOZ) graph that captures prior knowledge to guide object navigation agent with easier sub-goals.
- We propose a new evaluation metric named Success weighted by Action Efficiency (SAE).
- By integrating HOZ graph into a zone-to-action policy, the navigation performance can be significantly improved in SR, SPL and SAE metrics.

2. Related Work

**Geometry-based navigation:** Conventional navigation methods typically use a map as reference, whether it is constructed in advance or built simultaneously during visual navigation. [18, 4] utilize the metric-based map to perceive the environment and [12] keeps updating a probabilistic chessboard representation during agent’s locomotion. Comparatively, [36, 6, 5] adopt coarse-grained topological map, with nodes showing semantic features and edges reasoning spatial relationships. [37, 38] both integrate metric-based map and topological map to improve mobile robot navigation. [25] constructs an experience graph to deal with long-term appearance changes. In addition, [14] adopts a belief map as spatial memory. Rather than relying on a specific map, our HOZ graph acts as prior knowledge to aid navigation in unseen environments.

**Learning-based navigation:** Deep learning has gained popularity in end-to-end localization, exploration and so on [14, 36]. As an early try, [27] takes neural networks to build a hallway follower model in indoor navigation. Nowadays, many researches turn to reinforcement learning (RL) to help agents make action decisions [35, 4, 17]. To improve generalization, [44, 43, 41] all employ Actor-Critic model [30]. Moreover, [7] learns exploration policies using an intrinsic coverage reward in imitation learning. [24] trains a task generator and a meta-learner to learn transferable meta-skills. [8] uses a generative model with probabilistic framework to benefit the similarity calculation of two observations. [36, 2] propose a waypoint navigation to find simpler sub-goals. [32] utilizes semantic information to boost deeper understanding. Meanwhile, [13] puts forward a memory-based policy. They embed each observation into a memory and perform this spatial-temporal memory on three visual navigation tasks. [28] proposes a reachability estimator that provides the navigator a sequence of target observations to follow. This line of works mostly treat the policy network as a black box and train it via RL, whereas our HOZ graph includes coarse-to-fine inputs of object, region, and scene, which allows for interpretable navigation.

**Goal-driven navigation:** This kind of navigation is carried out for subjective purposes, mainly conducted by natural language instructions or target images. It can be distinguished into PointGoal navigation [14, 4] and ObjectGoal navigation [29, 13, 40, 32, 43, 41]. In particular, sometimes the target may be presented as an image [5, 44]. Our work focuses on object navigation in unseen indoor environments. [40] proposes a self-adaptive visual navigation method to help agent learn to learn in an unseen environment via meta-reinforcement learning. [11] proposes an object representation graph to learn the spatial correlations among different object categories, and uses imitation learning to train the agent. A memory-augmented tentative policy network is used to detect deadlock conditions.
Figure 2. Model Overview. Our model is composed of the hierarchical object-to-zone (HOZ) graph and the zone-to-action LSTM. Given the target object and current observations, the agent first recognizes the scene category, locates the current zone, and deduces the next sub-goal zone according to the HOZ graph. The HOZ graph is updated at each timestamp based on the observations of the unseen environment. The zone-to-action LSTM learns to predict efficient actions based on the concatenated information provided by the HOZ graph.

4. Hierarchical Object-to-Zone (HOZ) Graph

Our goal is to navigate agent to the given target without a precise map in the unseen environment. Thus, a great challenge in such task is to locate objects. Previous works [11, 40, 43] directly take the target object embedding as the goal to guide action prediction. However, it’s typically difficult to plan an efficient path without prior knowledge about the unknown environment. The agent in those works might not find the path at the beginning, leading to some meaningless actions, such as frequently spinning around and backing. In order to provide stronger guidance, our navigation model considers a wider range region where the target object may be located, which is denoted as zone.

Each zone usually consists of a group of relevant objects. For instance, microwave, cooker and sink usually appear in the same zone. Thus, navigating to microwave may first require locating such zone. Since precise map information is not available in the unseen environment, how to collect suitable zones information and construct a hierarchical object-to-zone (HOZ) graph remains challenging. Therefore, we start from seen scenes to construct HOZ graph (Section 4.1) and later adaptively update it when navigating in the unseen scenes (Section 4.2).

We consider the zones from the following hierarchical structure. Our environments consist of several scenes, such as bedroom, living room, and kitchen, etc, and each scene contains several rooms. In each room $i \in \{1, 2, \ldots, n\}$, we get room-wise HOZ graph $\Omega_i (V_i, E_i)$, whose zone nodes and provides additional action guidance during testing. Recent works have applied knowledge graphs to image classification [26], segmentation [45], zero-shot recognition [39] and navigation [43, 41]. [41] proposes Bayesian Relational Memory that captures the room-to-room prior layout of environments during training to produce sub-goals for semantic-goal visual navigation. [43] establishes an object-to-object graph by extracting the relationships among object categories in Visual Genome [22]. While in our work, we conduct the online-learning hierarchical object-to-zone (HOZ) graph to serve as prior knowledge for object navigation, which provides more general regional information.

3. Preliminary Notation

Considering a set of environments $Q$ and objects $P$, in each navigation episode, agent is initialized to a random location $l = \{x, z, \theta_{yaw}, \theta_{pitch}\}$ in an environment $q \in Q$. $x, z$ represent the plane coordinate and $\theta_{yaw}, \theta_{pitch}$ represent the yaw and pitch angle (of the agent). At each timestamp $t$, agent learns a policy function $\pi (a_t | o_t, p)$, which predicts an action $a_t \in \mathcal{A}$ based on first-person view $o_t$ and the target object $p \in P$. The discrete action space $\mathcal{A} = \{\text{MoveAhead}, \text{RotateLeft}, \text{RotateRight}, \text{LookDown}, \text{LookUp}, \text{Done}\}$. Note that the action $\text{Done}$ is judged by the agent itself rather than informed by the environment. The success of object navigation task requires agent finally capturing and getting close to the target object (less than a threshold).
Algorithm 1 Scene-wise HOZ graph construction

Input: (\( \text{Room}_1, \ldots, \text{Room}_n \)) of same scene category

1. Create room-wise HOZ graphs set \( \Omega \)
2. for \( i \leftarrow 1 \) to \( n \) do
3. Get features and locations \([(f_1, l_1), \ldots, (f_d, l_d)]\) in \( \text{Room}_i \) by agent with random exploring
4. Create a graph \( G_r(V_r, E_r) \)
5. \((C_1, \ldots, C_K) \leftarrow \text{K-Means}(f_1, \ldots, f_d, K)\)
6. \( E_r \leftarrow \) cluster centers \((C_1, \ldots, C_K)\)
7. \( E_r \leftarrow \) calculate edges with Equation 1
8. Add room-wise HOZ graph to \( \Omega_i \leftarrow G_r(V_r, E_r) \)
9. end for
10. Create scene-wise HOZ graph \( G_s(V_s, E_s) \)
11. Initialize \( G_s(V_s, E_s) \leftarrow \Omega_1 \)
12. for \( i \leftarrow 2 \) to \( n \) do
13. Create weighted bipartite graph \( G^b(V^b, E^b) \)
14. \( V^b \leftarrow V_s \) (all nodes of \( G_s \), \( V_i \) (all nodes of \( \Omega_i \))
15. \( \omega(E^b) \leftarrow \) calculate similarity by Equation 2
16. Perfect matching \( \Psi^* \leftarrow \text{Kuhn-Munkres}(\omega(E^b)) \)
17. Update \( G_s \leftarrow \text{Avg}(G_s, \Omega_i, \Psi^*) \) refer to Figure 3
18. end for

Output: scene-wise HOZ graph \( G_s(V_s, E_s) \)

are obtained by clustering the egocentric observation features and edges are defined as the adjacent probability of two zones (traced back to co-occurrence probability of each contained objects). Then we fuse these room-wise HOZ graphs grouped by scene to obtain scene-wise HOZ graphs \( G_s(V_s, E_s) \). All scene-wise HOZ graphs have the same structure and constitute our final HOZ graph (Section 4.1).

4.1. HOZ Graph Construction

4.1.1 Room-wise HOZ graph

Similar scenes (e.g. “living room”) may consist of common objects and object layouts [16, 46]. For instance, when referring to the living room, an area composed of sofa, pillow and table, or an area composed of TV set and TV cabinet may appear in our mind. When searching for an object, humans tend to first locate the typical area where the object most likely to appear. In our work, we denote such areas as zones and embed zones to guide agent. In order to obtain those representative zones, we sample visual features around the room and make a clustering on them.

In a specific room \( i \), we first let the agent explore the room to collect a set of visual tuple features \((f, l)\), where \( f \in \mathbb{R}^{N \times 1} \) is a bag-of-objects vector obtained by Faster-RCNN [34], representing the objects that appear in the current view. It should be noticed that we use the bag-of-objects vector composed of 0 and 1 to represent the object category. If the current view contains many objects belonging to the same category, we only record them once. \( N \) denotes the number of object categories, and \( l = \{x, z, \theta_{yaw}, \theta_{pitch}\} \) denotes the observation location defined in Section 3. Then we make K-Means clustering on features \( f \) to get \( K \) zones, forming the zone nodes in room-wise HOZ graph \( \Omega_i(V_r, E_r) \). We use \( v_k \) and \( \delta(v_k) \) to represent the \( k \)-th zone node and its embedded feature. The embedded feature represents the cluster center, which is calculated by \( \delta(v_k) = \frac{1}{|\text{zone}_k|} \sum_{(f, l) \in \text{zone}_k} f \), where \( \text{zone}_k \) is a group of clustered visual tuple features \((f, l)\) after K-Means, and \( |\text{zone}_k| \) is the element number. Each dimension’s value of \( \delta(v_k) \) shows the connection relationship between the zones layer and objects layer (Figure 2), representing the co-occurrence frequency of objects belonging to the \( \text{zone}_k \).

The edge \( e(v_k, v_j) \) in the zones layer, represents the probability that two zones are adjacent to each other, which can be calculated as follows:

\[
e(v_k, v_j) = \frac{\sum_{(f, l) \in \text{zone}_k} \sum_{(f', l') \in \text{zone}_j} \eta(l, l')}{|\text{zone}_k| \times |\text{zone}_j|}
\eta(l, l') = \begin{cases} 1 & |x_k - x_j| + |y_k - y_j| \leq \varepsilon \\ 0 & \text{otherwise} \end{cases}
\tag{1}
\]

where \( \varepsilon \) is a hyper-parameter threshold. Then we use all node features to recognize the scene category. For each room \( i \), we construct a room-wise HOZ graph \( \Omega_i(V_i, E_i) \).

4.1.2 Scene-wise HOZ graph

To obtain scene-wise HOZ graph, we group all room-wise HOZ graphs by scene category. Take one scene as an example, we can obtain the room-wise set \( \Omega = \{\Omega_1(V_1, E_1), \ldots, \Omega_n(V_n, E_n)\} \). Since the zones number \( K \) is fixed, each room-wise HOZ graph has the same structure for later matching and merging. Considering that directly computing the maximum matching of all room-wise HOZ nodes is expensive, we propose pairwise perfect matching and merging on two graphs each time until all graphs merge into the final one. The matching between \( \Omega_i(V_i, E_i) \) and \( \Omega_{i+1}(V_{i+1}, E_{i+1}) \) graphs can be regarded as the weighted bipartite graph matching. We construct a bipartite graph \( G^b(V^b, E^b) \), where \( V_i \) is the nodes set in \( \Omega_i \), \( |V_i| = |V_{i+1}| \), and \( E^b \) represents all fully connected edges. A perfect matching is to find a subset \( \Psi \subseteq E^b \), where each node has exactly one edge incident on it. The maximum perfect matching satisfies \( \Psi^* = \arg\max_{\Psi} \sum_{e \in \Psi} \omega(e^b) \), where \( e^b \equiv e^b(v_k, v_j) \) represents the edge matching nodes \( v_k, v_j \), \( v_k \in V_i, v_j \in V_{i+1} \). The weight function \( \omega(e^b) \) calculates the similarity of two nodes as

\[
\omega(e^b(v_k, v_j)) = 1/d(\delta_k, \delta_j)
\tag{2}
\]
For instance, two nodes (in red) are matched, and merged with average pooling. In this way, we can fuse room-wise HOZ graphs two-by-two. Following [11], we set up objects layer with objects as the input of GCN, where \( N \) are one-hot vectors that only activate representative nodes and relations between objects as edges, and encode the relative position to other zones. Which informs agent about the next sub-goal zone and its zone indicator vectors \( \delta \) with GCN. At time \( t = 0 \), the input matrix \( \delta (V^0) \in \mathbb{R}^{K \times N} \) represents embedded features for all zone nodes \( V \). Then \( \delta (V^t) \) will be updated based on \( f_t \), which can be formulated as

\[
\delta (V^t) = \lambda Z_c f_t^T + (I - \lambda Z_c Z_c^T) \delta (V^{t-1})
\]

where \( \lambda \) is a learnable parameter that determines the current observation’s impact on the general HOZ graph. Following [20], we perform normalization on edges \( E \) and obtain \( E_c \). With updated zone nodes \( \delta (V^t) \), adjacent relationship \( E_c \), our GCN outputs a node-level representation \( H_z \in \mathbb{R}^{K \times N} \) as the zones embedding

\[
H_z = \sigma (E_c (V^t) W_z)
\]

where \( \sigma (\cdot) \) denotes the ReLU activation function, and \( W_z \in \mathbb{R}^{N \times N} \) is the parameter of GCN layers. Then we take the encoded vector \( H_z^T Z_{sub} \) as the output of zones layer, which informs agent about the next sub-goal zone and its relative position to other zones.

4.2.2 Object Embedding

Following [11], we set up objects layer with objects as nodes and relations between objects as edges, and encode them with GCN. For current egocentric view, we can get the detection feature \( F_t = \{f_t^b, f_t^f, f_t^p\} \), where \( f_t^b \in \mathbb{R}^{N \times 4} \) is bounding box position, \( f_t^f \in \mathbb{R}^{N \times 1} \) is confidence score and \( f_t^p \in \mathbb{R}^{N \times 512} \) is the visual feature of objects. If multiple instances belonging to the same category appear simultaneously, the one with the highest confidence score provided by the detector will be selected. Define \( X_o = [f_t^p, f_t^f, p] \in \mathbb{R}^{N \times 6} \) as the input of GCN, where \( p \in \mathbb{R}^{N \times 1} \) is a one-hot vector representing the target object. The GCN outputs

\[
H_o = \sigma (A X_o W_o)
\]

Both the adjacency matrix \( A \) and the GCN network parameter \( W_o \in \mathbb{R}^{6 \times N} \) need to be learned. Then we integrate \( H_o f_t^p \) as the objects embedding, which provides object-level information.

5. Navigation Policy

5.1. Zone Localization and Navigation Planning

Current zone We compare current view bag-of-objects vector \( f_t \) with the nodes in the pre-learned HOZ graph.

\[
\frac{d (\delta_k, \delta_j)}{\sqrt{\delta_k \cdot \delta_j}} = \frac{1}{\delta_k + \delta_j}
\]

\[d (\delta_k, \delta_j) = \sqrt{\delta_k \cdot \delta_j} + \alpha\]

\[
\delta (v_k, v_j) = \delta (v_k) + \delta (v_j)
\]

\[d (\delta_k, \delta_j) = \sqrt{\delta_k \cdot \delta_j} + \frac{1}{\delta_k + \delta_j} + \alpha\]

\[d (\delta_k, \delta_j) = \sqrt{\delta_k \cdot \delta_j} + \frac{1}{\delta_k + \delta_j} + \alpha\]
After obtaining $\Gamma^*$, we can get the sub-goal zone $Z_{sub} = \chi^K(\tau_1^*)$. Whenever the current zone changes, the network will adaptively replan an optimal path and a sub-goal zone.

5.2. Policy Learning

**Action policy** The conventional works [40, 11, 43, 44] learn a policy $\pi(a_t|o_t, p)$ based on current observation. While in our work, we learn a zone-to-action LSTM action policy $\pi_z(a_t|S_t, p)$, where $S_t$ is the joint representation of current observation $o_t$, the sub-goal zone embedding $H^T_sZ_{sub}$ and object embedding $H_o f_{o_t}^p$. Following [44, 29] formulating this task as a reinforcement learning problem, we optimize the LSTM via the Asynchronous Advantage Actor-Critic (A3C) algorithm [30] that learns policy function and value function by minimizing navigation loss $L_{nav}$ to maximize the reward. The policy function outputs $a_t$, representing actions probability at each time, and the value function is used to train the policy network.

**Done reminder** To remind agent to stop in time when it encounters the target object, we propose the done reminder. Combining objects detection confidence $f_{o_t}^p$ and the target object $p$, we weight $a_t$ with $\beta p^T f_{o_t}^p$ to represent the effect of done action ($\beta$ is a learnable parameter). In this way, we can get the final action output $\hat{a}_t$.

6. Experiments

6.1. Experiment Setup

We evaluate our methods on AI2-Thor simulator [21], which provides near photo-realistic observation in 3D indoor scenes. AI2-Thor contains a total of 120 scenes in 4 types: living room, kitchen, bedroom, and bathroom, where spatial layout, object types and appearance are all different.
Ablation results of zone number. We evaluate the impact of the zone number (cluster number) on navigation metrics such as SR, SPL, and SAE.

Following the setting in [40], a subset of 22 types of objects is considered, ensuring that each scene contains at least four objects. For each scene type, we choose 20 rooms for training, 5 for validation, and 5 for test.

6.2. Implementation Details

The baseline is the A3C [30] navigation policy with a simple visual embedding layer to encode inputs. We train our models with 12 asynchronous workers, in a total of 6M navigation episodes. In policy learning, the agent receives a $-0.01$ penalty for each step and a reward of 5 if the episode is successful. We use Adam optimizer [19] to update our network parameters with a learning rate of $10^{-4}$. ResNet18 [15] pretrained on ImageNet [10] is used as our backbone to extract the features of each egocentric view. In the HOZ graph construction, we fine-tune Faster-RCNN [34] architecture on 50% training data of AI2-Thor. The hyper-parameters in our model are initialized to $\varepsilon = 0.25$, $\alpha = 0.1$ and $\beta = 0.6$.

For evaluation, we randomly select agent’s initial starting position and the target object, and repeatedly run 5 trials. We report results (with average and variance) for all targets (All) and a subset of targets ($L \geq 5$) whose optimal trajectory length is longer than 5.

6.3. Evaluation Metrics

We use Success Rate (SR), Success Weighted by Path Length (SPL) [1], and Success Weighted by Action efficiency (SAE) metrics to evaluate our model. SR refers to the success rate of agent in finding the target object, which is formulated as $SR = \frac{1}{N} \sum_{n=1}^{N} Suc_{n}$, where $N$ is the total number of episodes and $Suc_{n}$ is an indicator function to indicate whether the $n$-th episode succeeds. SPL considers both the success rate and the path length. It is defined as $SPL = \frac{1}{N} \sum_{i=1}^{N} Suc_{t} \left( \frac{L_{i}}{\max(L_{i}, L_{o})} \right)$, where $L_{i}$ is the actual path length and $L_{o}$ represents the shortest path provided by the simulator. Although SPL calculates the proximity between the path and the optimal path, it ignores the efficiency of action sequence. For instance, unnecessary rotations take time and reduce efficiency, which are not considered in SPL. Therefore, we propose the SAE metric to measure the efficiency of all actions. It is formulated as $SAE = \frac{1}{N} \sum_{i=1}^{N} Suc_{t} \frac{\sum_{t=0}^{T} (\mathbb{1}(a_{t} \in A_{\text{change}}))}{\sum_{t=0}^{T} (\mathbb{1}(a_{t} \in A_{\text{all}}))}$, where $\mathbb{1}(\cdot)$ is the indicator function, $a_{t}$ is agent’s action at time $t$ in episode $i$, $A_{\text{all}}$ is the set of all action categories and $A_{\text{change}}$ refers to those actions that can change agent’s location. In our settings $A_{\text{change}} = \{\text{MoveAhead}\}$.

6.4. Ablation Study

Effectiveness of sub-goal zones As discussed in Section 5.1, besides the target zone, we also consider the sub-goal zone. The ablation study respectively trains the policy network with the sub-goal zone and the target zone as illustrated in Table 6 line2 and line4. Compared to the target zone, sub-goal zone can better guide agent efficiently. Training with the embedding of sub-goal zone outperforms target zone by 1.41/1.24, 1.79/1.85 and 1.15/0.53 in SR, SPL and SAE (ALL/$L \geq 5$, %) respectively.

Impacts of the number of zones The cluster number is a hyper-parameter that specifies the zone number in a scene. Figure 5 indicates that performance is reduced when the number of zones is either too large or too small. Besides, a large zone number requires significant computing resources when planning the path. The results suggest that the optimal number of zones is 8. Therefore, the number of zones is set to 8 in the remaining evaluations.

Other ablation studies We dissec the proposed HOZ graph into different components. The ablation study in Table 2 demonstrates the efficacy of each component of our method. Specifically, it is observed that the object layer significantly improves the baseline performance. Additionally, scene and zone layers can considerably increase the performance on SPL and SAE metrics. Although the done
Table 2. The ablation study of different components (\%). We evaluate the effect of various modules. These modules include the scene layer (Scene), the zone layer (Zone), the object layer (Object) in Section 4.2 and the done reminder (Reminder) in Section 5.2.

| Baseline | Scene | Zone | Object | Reminder | SR | SPL | SAE | SR | SPL | SAE |
|----------|-------|------|--------|----------|----|-----|-----|----|-----|-----|
|          |       |      |        |          |    |     |     |    |     |     |
| ✓        |       |      |        |          | 57.35 ±1.92 | 33.78 ±1.33 | 20.04 ±1.36 | 45.77 ±2.17 | 30.65 ±1.01 | 20.04 ±1.87 |
| ✓        | ✓     |      |        |          | 65.12 ±1.03 | 23.06 ±0.91 | 19.78 ±0.78 | 53.42 ±1.43 | 35.37 ±0.71 | 25.32 ±1.04 |
| ✓        | ✓     | ✓    |        |          | 65.81 ±1.11 | 23.06 ±0.91 | 24.81 ±0.84 | 57.23 ±0.93 | 36.25 ±0.65 | 25.53 ±0.87 |
| ✓        | ✓     | ✓    | ✓      |          | 66.73 ±1.01 | 23.06 ±0.91 | 24.81 ±0.84 | 57.55 ±1.19 | 36.48 ±0.52 | 27.72 ±1.07 |
| ✓        | ✓     | ✓    | ✓      | ✓        | 70.57 ±1.11 | 23.06 ±0.91 | 27.19 ±1.96 | 61.52 ±1.47 | 40.46 ±0.63 | 29.61 ±1.08 |
| ✓        | ✓     | ✓    | ✓      | ✓        | 70.62 ±1.70 | 23.06 ±0.91 | 27.97 ±2.01 | 62.75 ±1.73 | 39.24 ±0.56 | 30.14 ±1.34 |

Table 3. Comparisons with the related works (%). Constrained by space, variance is detailed in supplementary materials.

| Method               | All | L ≥ 5 |
|----------------------|-----|-------|
|                      | SR  | SPL   | SAE  | SR  | SPL   | SAE  |
| Non-adaptive method  |     |       |      |     |       |      |
| Random               | 3.56| 1.73  | 0.41 | 0.27| 0.07  | 0.06 |
| A3C (baseline)       | 57.35| 33.78 | 19.02| 45.77| 30.65 | 20.04|
| SP [43]              | 62.16| 37.01 | 23.39| 50.86| 34.17 | 24.35|
| ORG [11]             | 66.38| 38.42 | 25.36| 55.55| 36.26 | 27.53|
| Ours (HOZ)           | 70.62| 40.02 | 27.97| 62.75| 39.24 | 30.14|
| Self-supervised method |   |       |      |     |       |      |
| SAVN [40]            | 63.32| 37.62 | 21.97| 52.38| 35.31 | 24.64|
| ORG-TPN [11]         | 67.31| 39.53 | 23.07| 57.41| 38.27 | 26.37|
| Ours (HOZ-TPN)       | 73.15| 39.22 | 29.49| 64.58| 39.80 | 30.92|

remind the agent to locate the current zone and offers guidance from the current zone to the target zone, thus the agent has better performance. Notably, with the guidance of sub-goal zone, the agent equipped with HOZ graph can choose a better rotation direction than the baseline method.

**Case study** Figure 4 qualitatively compares our HOZ with the baseline model. In these scenarios, the agent is placed at an initial position where the target object cannot be seen. The baseline model often falls into rotations when the target object is not in the view. However, our HOZ method helps the agent locate the current zone and offers guidance from the current zone to the target zone, thus the agent has better performance. Notably, with the guidance of sub-goal zone, the agent equipped with HOZ graph can choose a better rotation direction than the baseline method.

**7. Conclusions**

We propose the hierarchical object-to-zone (HOZ) graph that captures the prior knowledge of objects in typical zones. The agent equipped with HOZ is capable of updating prior knowledge, locating the target zone and planning the zone-to-zone path. We also propose a new evaluation metric named Success weighted by Action Efficiency (SAE) that measures the efficiency of actions. Experimental results show that our approach outperforms baseline by a large margin in SR, SPL and SAE metrics.

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A. Video Demo

A video demo that visualizes the construction of HOZ graph, navigation with HOZ graph and more case studies can be found at the following url: https://drive.google.com/file/d/1UtTcFRhF2FLKqgaiKom6_9GpQmsJfhXAZC/view?usp=sharing

B. Navigation Target

The target objects of different scenes in AI2THOR [21] are shown in Table 4. Our training and testing share the consistent target objects categories, though the testing environments are new and unseen.

Considering that each environment in AI2THOR usually contains one room, the agent navigation may be limited to short trajectories. Thus, for longer trajectories object navigation, we also conduct experiments on a more complex simulator RoboTHOR [9], which has 2.4 times larger area and 5.5 times longer trajectory length than AI2THOR. The environment in RoboTHOR usually contains a variety of rooms. To highlight the differences between AI2THOR and RoboTHOR, we define each environment in AI2THOR as room and that in RoboTHOR as apartment. In RoboTHOR, 12 objects categories are selected as target objects for training and testing, involving Book, Bowl, Chair, Plate, Television, Floor Lamp, Garbage Can, Alarm Clock, Desk Lamp, Laptop, Pot, CellPhone. The experimental results are shown in Section D.1.

C. More Ablation Studies

C.1. Clustering information

In our method, we sample a set of features \((f, l)\) according to the observations in the environments, where \(f\) is a bag-of-objects vector representing objects categories detected in view, and \(l\) represents the sample location. Then we implement feature clustering on \(f\), and each obtained cluster serves as a zone node in room-wise HOZ. That is to say, our zone node is only based on visual information. In order to further explore the impact of clustering, we introduce the additional location information and cluster on both \((f, l)\). Table 5 demonstrates the navigation performance with these two clustering methods. The results show that clustering on both visual and location information drops 2.40/2.12\% and 2.16/1.05\% in SR and SAE and slightly improves in SPL, suggesting that the additional location information narrows the range of our proposed zone. In other words, our HOZ (clustering on visual information) treats all regions where agent can observe similar objects with a specified direction as a zone, while clustering with both visual and location information restrains the zone region merely around these objects. Thus, location is more like a constraint rather than helpful information, limiting the visual generalization of the proposed HOZ graph. When the target object is not in view, agent needs to search more zones until discovering the target. It is obviously inefficient so that we obtain zone nodes for HOZ only based on visual information.

C.2. Object detection module

Table 6 shows the impact of different detection modules on navigation performance, where Detection Pre indicates that the detection module is pre-trained with labeled egocentric images sampled in simulator, and Detection GT indicates that the detection module is ground truth provided by simulator. The ablation with ground truth detection improves performance by 1.66/1.60, 2.37/4.91 and 18.05/13.36 in SR, SAE and SPL (ALL/L ≥ 5, %) respec-
Table 5. Comparisons with different information used for clustering (%). The zone clustering is based on different information, including visual information (Visual) and location information (Location).

| Visual | Location | ALL SR | SPL | SAE | ALL SR | SPL | SAE |
|--------|----------|--------|-----|-----|--------|-----|-----|
| √      |          | 70.62 ± 1.70  | 40.02 ± 1.25 | 27.97 ± 2.01 | 62.75 ± 1.73 | 39.24 ± 0.56 | 30.14 ± 1.34 |
| √      | √        | 68.22 ± 1.54  | 40.48 ± 1.07 | 25.81 ± 1.78 | 60.63 ± 1.46 | 37.92 ± 0.48 | 29.09 ± 1.01 |

Table 6. Comparisons with different detection modules (%). We compare the impact of utilizing a pre-trained detection model (Detection Pre) or the ground truth of object detection (Detection GT).

| Module       | ALL SR | SPL | SAE | ALL SR | SPL | SAE |
|--------------|--------|-----|-----|--------|-----|-----|
| Detection Pre | 65.12 ± 1.03 | 37.86 ± 0.93 | 24.36 ± 0.91 | 53.42 ± 1.43 | 35.37 ± 0.71 | 25.32 ± 1.04 |
| Detection GT  | 66.78 ± 0.73 | 55.91 ± 0.46 | 26.73 ± 0.26 | 55.02 ± 0.68 | 48.73 ± 0.31 | 30.23 ± 0.33 |

tively. The results demonstrate that accurately recognizing more objects can help agent navigate successfully in shorter trajectories. It is easy to understand because agent can take the most likely action at each step to obtain the high SPL. However, since the navigation task includes multiple decision steps, its success rate does not rely on taking the perfect action at each step. As long as most actions are reasonable, the agent can still achieve success. So the approximate results on SR and SAE indicate that our HOZ graph still makes sense in guiding unseen object navigation.

C.3. The ablations of graph settings

Since our HOZ graph adds more parameters to the model, we perform additional ablations of zone nodes and edges, as indicated in Table 7. To assess if the gain in network performance is due to the increased number of parameters or the information contained in the HOZ graph’s nodes and edges, We respectively set the edges and nodes of the HOZ graph to random. The experimental results show that the control experiments with random settings perform worse than the original value, demonstrating the efficacy of zone information (nodes) and spatial priors (edges).

D. More comparisons with the related works

D.1. Experiments on RoboTHOR

For longer trajectories object navigation, we also conduct experiments on RoboTHOR [9] simulator. RoboTHOR consists of 89 apartments, 75 for training and validation, while the testing data have not yet been made public. Therefore, we choose 60 apartments for training, 5 for validation and 10 for testing. Since the regions in RoboTHOR are simply separated with several clapboard, we treat each apartment as a whole rather than subdividing it into scattered scenes. Therefore, different from the construction of scene-wise HOZ graph in AI2THOR, we build apartment-wise HOZ graph in RoboTHOR and establish a unified HOZ graph combing all apartments.

Table 8 illustrates that our method still outperforms the state-of-the-art with a large margin by 2.66/2.30 in SR, 1.25/1.16 in SPL and 2.46/1.80 in SAE metric (ALL/L ≥ 5, %). Besides, compared with self-supervised methods, our method equipped with the equal self-supervised adaptive module also gains significant improvement of 3.27/2.73 in SR, 1.62/1.41 in SPL and 2.14/1.74 in SAE metric (ALL/L ≥ 5, %).

In addition, we supplement the experimental results of variance for Table 3 in the main text. The complete experimental results are shown in Table 9.

D.2. Comparisons with semantic map

In addition, Chaplot et al. [3] attempt to construct the episodic semantic map and use it to explore the unseen environment. Different from our method that only relies on RGB input, the semantic map is constructed based on a variety of inputs, including RGB-D input, segmentation mask.
**Table 7. More ablations of graph settings (%)**. The parameters of nodes or edges are randomly set (R) or kept (K).

| Nodes | Edges | SR   | SPL  | SAE  | SR   | SPL  | SAE  |
|-------|-------|------|------|------|------|------|------|
|       |       | ALL  |       |      |      |      |      |
| R     |       | 67.81±0.62 | 38.92±0.22 | 24.13±0.35 | 57.84±0.81 | 38.22±0.44 | 24.02±0.52 |
| K     |       | 68.52±1.05 | 39.83±0.52 | 26.52±0.62 | 58.61±0.82 | 38.73±0.62 | 28.73±0.53 |
| K     | R     | 69.33±0.32 | 39.71±0.32 | 26.63±0.13 | 59.93±0.53 | 39.14±0.45 | 29.01±0.312 |
| K     | K     | 70.47±0.35 | 40.66±0.47 | 27.85±0.44 | 62.17±0.26 | 40.14±0.46 | 30.33±0.25 |

**Figure 7. Visualization of trajectory in RoboTHOR.** Black arrows represent rotations. The trajectory of the agent is illustrated with green and blue arrows, where green is the beginning and blue is the end.
Table 8. Comparisons with the related works in RoboTHOR [9] (%). We repeat the evaluations similar to A12-Thor on RoboTHOR.

| Method          | SR    | ALL SPL | SAE    | SR   | L ≥ 5 SPL | SAE   |
|-----------------|-------|---------|--------|------|-----------|-------|
| Non-adaptive method |       |         |        |      |           |       |
| Random          | 0.00±0.00 | 0.00±0.00 | 0.00±0.00 | 0.00±0.00 | 0.00±0.00 | 0.00±0.00 |
| A3C (baseline)  | 26.41±0.52 | 16.61±0.34 | 13.15±0.43 | 17.42±0.21 | 12.23±0.66 | 10.94±0.35 |
| SP [43]         | 28.04±0.33 | 17.63±0.26 | 14.23±0.25 | 21.66±0.32 | 15.14±0.46 | 13.27±0.34 |
| ORG [11]        | 29.61±0.71 | 19.23±0.94 | 14.72±0.64 | 22.53±0.55 | 15.73±0.86 | 13.82±0.44 |
| Ours (HOZ)      | 32.27±1.14 | 20.48±0.63 | 17.18±0.42 | 24.83±0.72 | 16.89±0.50 | 15.62±0.55 |

| Self-supervised method |       |         |        |      |           |       |
|------------------------|-------|---------|--------|------|-----------|-------|
| SAVN [40]              | 28.42±0.41 | 17.82±0.33 | 13.91±0.24 | 22.13±0.32 | 15.34±0.45 | 13.01±0.24 |
| ORG-TPN [11]           | 30.01±1.22 | 20.51±0.74 | 14.52±0.93 | 22.25±0.63 | 16.64±0.35 | 13.83±0.45 |
| Ours (HOZ-TPN)         | 33.28±1.62 | 22.13±0.91 | 16.66±0.62 | 24.98±1.32 | 18.05±0.64 | 15.57±0.76 |

Table 9. Comparisons with the related works in A12THOR (%). These results are the supplement for Table 3 in the main text.

| Method          | Suc. All SPL | SAE | Suc. L ≥ 5 SPL | SAE |
|-----------------|--------------|-----|----------------|-----|
| Non-adaptive method |             |     |                |     |
| Random          | 3.56±2.74 | 1.73±1.52 | 0.41±0.52 | 0.27±0.22 | 0.07±0.06 | 0.06±0.05 |
| A3C (baseline)  | 57.35±1.92 | 33.78±1.33 | 19.02±1.36 | 45.77±2.17 | 30.65±1.01 | 20.04±1.87 |
| SP [43]         | 62.16±0.70 | 37.01±0.68 | 23.39±0.69 | 50.86±0.34 | 34.17±0.85 | 24.35±0.74 |
| ORG [11]        | 66.38±0.95 | 38.42±0.22 | 25.36±0.43 | 55.55±1.89 | 36.26±0.39 | 27.53±0.48 |
| Ours (HOZ)      | 70.62±1.70 | 40.02±1.25 | 27.97±2.01 | 62.75±1.73 | 39.24±0.56 | 30.14±1.34 |

| Self-supervised method |     |     |               |     |
|------------------------|-----|-----|---------------|-----|
| SAVN [40]              | 63.32±1.17 | 37.62±0.86 | 21.97±0.21 | 52.38±0.73 | 35.31±0.79 | 24.64±0.52 |
| ORG-TPN [11]           | 67.31±1.14 | 39.53±1.01 | 23.07±1.24 | 57.41±0.71 | 38.27±0.63 | 26.37±0.57 |
| Ours (HOZ-TPN)         | 73.15±1.01 | 39.22±1.27 | 29.49±1.11 | 64.58±0.74 | 39.80±0.57 | 30.92±0.40 |

Table 10. Comparisons with the semantic map in Gibson (%). The baseline is the A3C model with a simple visual embedding layer to encode various inputs. Since the path lengths of all episodes are larger than 5, the subset of $L ≥ 5$ is excluded.

| Method          | SR   | SPL | SAE |
|-----------------|------|-----|-----|
| Baseline + HOZ  | 43.47±0.51 | 12.88±0.36 | 11.67±0.51 |
| SemExp [3]      | 44.01±0.47 | 14.34±0.42 | 12.32±0.43 |
| SemExp + HOZ    | 45.19±0.35 | 14.68±0.38 | 12.73±0.45 |

E. Qualitative Results

E.1. The HOZ graph visualization

Figure 6 illustrates the visualization of our HOZ graph. We visualize the zones nodes in a scene-wise HOZ graph (e.g., living room), which is the fusion of 20 room-wise HOZ graphs. There are 8 zones marked with different colors and each zone consists of similar objects distribution. Even though there are overlapped objects among zones, each zone has semantically representative objects. For instance, in Figure 6, $zone_2$, $zone_3$, $zone_6$ focus on laptop, garbage can and television, respectively.

E.2. Navigation trajectory

Figure 7 qualitatively compares our method with the baseline in RoboTHOR. Benefiting from the sub-goals guidance and online-updating of proposed HOZ graph, agent can still adopt reasonable actions even in the long trajectory unseen navigation task, while the baseline model often falls into confusion and struggles with spinning around.