Phase-resolved Higgs response in superconducting cuprates

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In high-energy physics, the Higgs field couples to gauge bosons and fermions and gives mass to their elementary excitations. Experimentally, such couplings can be inferred from the decay product of the Higgs boson, i.e., the scalar (amplitude) excitation of the Higgs field. In superconductors, Cooper pairs bear a close analogy to the Higgs field. Interaction between the Cooper pairs and other degrees of freedom provides dissipation channels for the amplitude mode, which may reveal important information about the microscopic pairing mechanism. To this end, we investigate the Higgs (amplitude) mode of several cuprate thin films using phase-resolved terahertz third harmonic generation (THG). In addition to the heavily damped Higgs mode itself, we observe a universal jump in the phase of the driven Higgs oscillation as well as a non-vanishing THG above $T_c$. These findings indicate coupling of the Higgs mode to other collective modes and potentially a nonzero pairing amplitude above $T_c$.
For field theories with U(1) continuous symmetry and respecting Lorentz invariance or particle-hole symmetry, spontaneous symmetry breaking gives rise to an order parameter with two orthogonal collective modes: the Goldstone mode along the azimuthal direction, and the Higgs mode along the radial direction. In superconductors, discussions about the Higgs mode and the Higgs mechanism precede those in high-energy physics. However, their significance to superconductivity has been more slowly appreciated. Experimental detection of the Higgs mode has also been hampered by its lack of electric and magnetic dipole moments in most superconductors. Recently, it was proposed that the Higgs mode may reveal the superconducting gap symmetry and multiplicity, unveil coupled collective modes, or explain aspects of light-induced superconductivity. Novel methods for exciting and detecting the superconducting Higgs mode were also demonstrated using ultrafast terahertz techniques in the meantime. Specifically, free oscillations of the Higgs mode, with its characteristic frequency of $2\Delta$, can be launched by an ultrashort terahertz pulse quenching the free energy of the order parameter. Alternatively, it could also be periodically driven at $2\omega$ through nonlinear coupling between the electromagnetic vector potential $A(\omega)$ and the superconducting condensate. The resulting free (driven) Higgs oscillation manifests itself in terahertz transmissivity as an oscillation at $2\Delta$ ($2\omega$). In the latter scenario, the $2\omega$ oscillation of the condensate interacts with the driving field $A(\omega)$, leading to sum frequency generation or third harmonic generation (THG), which is resonantly enhanced when $2\omega = 2\Delta(T)$. While both free and driven Higgs oscillations have been demonstrated in s-wave superconductors, the Higgs mode of d-wave superconductors is more complex. The continuous variation of $\Delta$ between 0 and $\Delta_{\text{max}}$ along different directions of the Brillouin zone leads to strong dephasing of the mode. This is compounded by the existence of quasiparticle excitations at arbitrarily low energies, which provide rapid decay channels and significantly damp the mode. Terahertz pump optical probe experiments on Bi$_2$Sr$_2$CaCu$_2$O$_{8+y}$ single crystals have provided the first experimental evidence for an isotropic Higgs response of d-wave superconductors in the form of an $|A|^2$ response in the condensate's optical reflectivity to a monocyte terahertz pulse. On the other hand, periodically driving the Higgs oscillation would provide useful phase information that may indicate resonance and coupling to other modes. Such an experiment requires a multicycle, carrier-envelope phase-stable terahertz source with a narrow bandwidth and high electric field strength, which is provided by the TELBE superradiant undulator source at HZDR. Using this facility, we investigate the THG response of optimally-doped $\text{La}_{1.84}\text{Sr}_{0.16}\text{CuO}_4$ ($T_c = 45$ K), $\text{DyBa}_2\text{Cu}_3\text{O}_7$ ($T_c = 90$ K), $\text{YBa}_2\text{Cu}_3\text{O}_7$ ($T_c = 88$ K), and overdoped Bi$_2$Sr$_2$CaCu$_2$O$_{8+\delta}$ ($T_c = 65$ K) thin films (Supplementary Note 1). Our experiment is performed with 0.7 THz driving frequency, with an electric field up to $-50$ kV cm$^{-1}$ (Supplementary Note 2). In all of these samples, we observe an increase in THG intensity ($I_{\text{THG}}$) below $T_c$ that is consistent with a heavily damped Higgs oscillation. In addition, in LSCO(OP45), DyBCO(OP90) and YBCO (OP88), a universal jump in the relative phase between the THG response and the linear drive ($\Phi_{\text{TH}}$) at $T < T_c$ is observed, signifying the coupling of the Higgs mode to another collective mode. We also observe a nonzero $I_{\text{THH}}$ persisting above $T_c$ in all of the samples, which may indicate preformed Cooper pairs above $T_c$.

**Results**

**THG response of d-wave superconductors.** To illustrate the THG response of d-wave superconductors, first we show terahertz transmission through LSCO(OP45). As Fig. 1a–d shows, while the residual fundamental harmonic (FH) dominates the terahertz transmission above $T_c$, a large amplitude of third harmonic (TH) becomes visible below $T_c$. Moreover, FH transmission ($I_{\text{FH}}$) monotonically decreases with decreasing temperature as shown in Fig. 1e. In comparison, TH intensity ($I_{\text{THG}}$) exhibits a maximum below $T_c$. In the context of superconductors, the nonlinear Meissner effect, charge density fluctuations (CDF), and

![Fig. 1 THG from driven Higgs oscillation in LSCO(OP45). a, b Terahertz field transmitted through LSCO(OP45) at 90 K and 28 K. A 2.1 THz bandpass filter is placed after the sample to suppress the 0.7 THz transmission (Supplementary Note 2). c, d 0.7 THz fundamental harmonic (FH) and 2.1 THz third harmonic (TH) extracted from b using 1.4 THz FFT low pass and high pass filters. e FFT power spectrum of the transmitted field at selected temperatures across $T_c = 45$ K. f Transmitted FH and TH power versus incoming FH field at 28 K. Solid lines are guides-to-the-eye with a slope of 2 and 6.]
**Discussion**

To obtain an intuitive understanding of the phase response, we look at a driven coupled harmonic oscillators model. Whereas isolated oscillators exhibit a maximum in their amplitude and a positive phase jump \( \pi \) across resonance (Supplementary Note 8), the coupled oscillators system develops an anti-resonance in addition to resonances. This manifests as a minimum in the amplitude of the driven oscillator, simultaneous with a phase jump in the negative direction (Fig. 4a). To more closely model our experiment, we fix the driving frequency but allow the energetics of the oscillators to depend on temperature (Fig. 4b) (Supplementary Note 8). By choosing their resonance frequencies...
as $\Delta(T)$ and $\delta\Delta(T)$ ($\delta < 1$), where $\Delta(T) = \sqrt{n_i(T)}$ ($n_i$ is the experimentally measured superfluid density in LSCO(OP45)), the model recaptures the essential features of LSCO(OP45) (Fig. 3a, d). In YBCO(OP88) a smaller dip in $I_{TH}$ (T) is seen while in DyBCO(OP90) a kink in $I_{TH}$ (T) is observed at the $T_c$. This could be due to the sharpness of the phase jump in these two samples, causing the dip in $I_{TH}$ (T) to be very narrow in temperature and buried between the measured temperature points. In the framework of the coupled oscillators model, this suggests that the coupled mode is less damped in the bilayer systems compared to the single-layer LSCO(OP45). A classical Fresnel analysis of the thin film effects excludes the possibility of the phase jump coming from linear shifts in $\Phi_{TH}$ (T) and $\Phi_{FH}$ (T) (Supplementary Note 5).

While our classical toy model does not aim to explain the microscopic origin of the observed THG response, it allows us to learn about the dynamics and energetics of the coupled mode. It suggests that the coupled mode is underdamped and has an energy scale comparable to the Higgs mode. Moreover, the energy of this mode and/or its coupling to the Higgs mode depends on temperature. Within these constraints, potential candidates for the coupled collective mode include paramagnons, collective charge fluctuations of the incipient charge density wave (CDW) order, or phonons. In particular, coupling between the Higgs mode and CDW excitations has been observed in NbSe$_2$ and 2H-TaS$_2$ superconductors. In cuprates, charge order exhibits a similar energy scale as the superconducting gap. Evidence for the incipient charge order in a wide range of the phase diagram has also been reported. On the other hand, paramagnons are strongly renormalized in the superconducting state into a sharp underdamped resonance mode in a similar energy window as the superconducting gap. They are prominent candidates for mediating Cooper pairing in high-$T_c$ superconductors. Last but not least, strong electron-phonon coupling may also contribute a phononic character to the superconducting order parameter, leading to new amplitude mode(s) in the Higgs response. Other exotic but potential candidates include the Bardasis-Schrieffer mode and the anisotropic $A_{2g}$/B$_{1g}$ Higgs mode (Supplementary Note 9), which are also collective modes of the superconducting order parameter. Future doping and magnetic field dependence studies may shed light on the identity of the coupled mode.

While the identity of the coupled mode demands further scrutiny, our experiment also reveals a non-vanishing THG response above $T_c$ in all samples. In Fig. 4c, we plot the temperature dependence of $(I_{TH}/I_{FH})^{1/4}$, which is theoretically predicted to be $\propto \Delta$ away from resonance. Indeed, $(I_{TH}/I_{FH})^{1/4}$ exhibits an order parameter-like temperature dependence below $T_c$. Surprisingly, it remains nonzero up to $T > 1.5 T_c$, similar to the temperature regime where superconducting fluctuations are observed in Nernst effect measurements. This is more clearly illustrated by the transmitted TH waveform from LSCO(OP45) at $T = 50 K > T_c$ (Fig. 4d). Our observation may indicate preformed Cooper pairs in cuprates without global phase coherence, or the intense terahertz field might enforce phase coherence above $T_c$. The pseudogap, and its various ordered phases including the CDW order, may also play a role in THG above $T_c$.

While the coupled oscillators model offers an intuitive explanation for the unexpected phase jump in THG in several families of cuprates, it is a classical toy model and calls for a full quantum mechanical treatment of the subject to provide deeper insight. In parallel, future magnetic field and doping dependence investigations may further help unveil the nature of the coupled mode and the non-vanishing THG response above $T_c$. Sweeping the driving frequency may also help distinguish the different scenarios of $d$-wave gap closing or filling as temperature approaches $T_c$. While these initiatives are underway, our technique may also serve as a probe for non-equilibrium superconductivity. With so many interesting prospects, we see a bright future for phase-resolved spectroscopy of collective modes in superconductors and beyond.

**Fig. 3 Temperature dependence of TH intensity ($I_{TH}$) and relative phase ($\Phi_{FH}$) from optimally-doped cuprates. a-c Temperature dependence of TH intensity, $I_{TH}$ (blue), and normalized TH intensity, $I_{TH}/I_{FH}$ (gray), in LSCO(OP45), DyBCO(OP90) and YBCO(OP88). d-f Temperature dependence of the relative phase between the TH response and the FH drive, extracted from waveforms such as those in Fig. 1c, d. Inset shows representative TH waveforms across the $\pi$ phase jump temperature ($T_a$). The dotted line (black) denotes $T_c$ and the solid line (red) denotes $T_a$. The error bars represent the two sigma uncertainty from fitting the phase of TH and FH waveforms (Supplementary Note 4).**
Δ

oscillator and an underdamped harmonic oscillator as the driving frequency \( \omega \) is varied. When these two oscillators are coupled, the coupled system retains two resonances but also develops an anti-resonance. Across the anti-resonance (vertical dotted line), the amplitude (solid red line) of the driven oscillator goes through a minimum while its phase (solid blue line) jumps negatively with the driving frequency. a Assuming the driving frequency is fixed as in our experiment, but that the resonance frequency of the two oscillators varies with temperature as \( \Delta(T) \) and \( \delta\Delta(T) (6 < 1) \), the response of the coupled oscillators system is shown as a function of \( T \). The anti-resonance in \( a \) is recaptured: the amplitude of the Higgs oscillation (thin red line) goes through a minimum while its phase (thick blue line) jumps negatively with \( T \). The dotted line illustrates the effect of screening, which is to reduce the driving force and hence the amplitude at lower \( T \). c Temperature dependence of \( (I_{TH}/I_{FH})^{1/4} \), which remains finite above \( T_c \). (\( I_{TH}/I_{FH} \))\(^{1/4}\) is theoretically predicted to be \( \propto \Delta \) away from resonance. d FH and TH components extracted from the transmitted waveform from LSCO(OP45) at 50 K > \( T_c \).

### Methods

**Sample growth and characterization.**

The LSCO(OP45) and DyBCO(OP90) samples were grown by molecular beam epitaxy (MBE), and the YBCO(OP88) sample was grown by pulsed laser deposition (PLD) at the Max Planck Institute for Solid State Research. The LSCO(OP45) sample is 80 nm-thick on a LaSrAlO\(_4\) (LSAO) substrate. The DyBCO(OP90) sample is 70 nm-thick on a (LaA\(_{0.3}\)Sr\(_{2}\)TaAlO\(_6\))\(_{0.7}\)(LSAT) substrate. The YBCO(OP88) sample is 200 nm-thick on a NdGaO\(_3\) (NGO) substrate. The BSCCO(OD65) sample was grown by sputtering technique at Laboratoire de Physique des Solides. The BSCCO(OD65) sample is 160 nm thick on a MgO substrate. As shown in Supplementary Note 1, \( T_c \) is determined from mutual inductance measurement for LSCO(OP45), DyBCO (OP90) and YBCO(OP88). \( T_c \) of BSCCO(OD65) is determined from the drop in magnetic moment from SQUID measurement under zero-field cooling. We define \( T_c \) as the onset of the drop in mutual inductance and magnetic moment during cooling.

**THG experiment.** The majority of the data presented in this study are measured using the experimental setup shown in Supplementary Note 2. For fluorescence dependence measurements, we add an additional 1.93 THz bandpass filter (BPF) before Polarizer 3 (P3) to suppress the fundamental harmonic (FH). For temperature dependence of third harmonic (TH) in BSCCO(OD65), we also add an additional 1.9 THz BPF before P3. For electro-optical sampling we used a 2 mm ZnTe crystal and 100 fs gate pulse with 800 nm central wavelength. Accelerator-based THz pump and the laser gating pulse have a timing jitter characterized by a standard deviation of \( \pm 20 \) fs. Synchronization was achieved through pulse-resolved detection.

**Data availability**

The data that support the findings of this study are available from the first author and the corresponding authors upon reasonable request. The raw pre-sorted and pre-binned data that allow statistical analysis is available at https://doi.org/10.14278/rodare.277 together with the software tools that were used for data treatment. Further requests on data treatment should be sent to HZDR via S.Ko.

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Author contributions

S.Ka., R.S., Z.W., M.G., D.M., A.S. conceived the project. S.Ka., R.S., H.C., S.Ko., M.G. developed the experimental plan. S.Ko. built the setup at the TELBE facility. Data was taken and evaluated together with S.G., J.-C.D., N.A., I.L., B.G., M.C., M.B., M.G., Z.W., H.C., M.-J.K., K.K., R.D.D., N.Y., R.S., and S.Ka. R.D.D., K.K., H.C., M.-J.K., A.Y.B. conducted London penetration depth measurements. H.C., K.K., M.-J.K., R.D.D., N.Y., Z.W. performed data analysis and interpreted the results together with S.Ka., A.S., R.S., and B.K. I.S., H.C. performed theoretical modeling, G.K., D.P., Z.Z.L., H.R., G.C., G.L., Y. G. provided and characterized samples. H.C. together with A.S. and S.Ka. wrote the manuscript with inputs from all authors.

Competing interests

The authors declare no competing interests.

Additional information

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