Chromatin interaction studies can reveal how the genome is organized into spatially confined sub-compartments in the nucleus. However, accurately identifying sub-compartments from chromatin interaction data remains a challenge in computational biology. Here, we present Sub-Compartment Identifier (SCI), an algorithm that uses graph embedding followed by unsupervised learning to predict sub-compartments using Hi-C chromatin interaction data. We find that the network topological centrality and clustering performance of SCI sub-compartment predictions are superior to those of hidden Markov model (HMM) sub-compartment predictions. Moreover, using orthogonal Chromatin Interaction Analysis by in-situ Paired-End Tag Sequencing (ChIA-PET) data, we confirmed that SCI sub-compartment prediction outperforms HMM. We show that SCI-predicted sub-compartments have distinct epigenetic marks, transcriptional activities, and transcription factor enrichment. Moreover, we present a deep neural network to predict sub-compartments using epigenome, replication timing, and sequence data. Our neural network predicts more accurate sub-compartment predictions when SCI-determined sub-compartments are used as labels for training.
The genome is hierarchically organized in three-dimensional (3D) space, and chromosomal sequences can be mapped to one of two major compartments: compartment A is associated with open chromatin, and compartment B is associated with closed chromatin. The A/B compartments are predicted from chromatin interaction data, in particular, data generated by the genome-wide Hi-C chromatin interaction profiling technique, which combines proximity-based ligation with massively parallel sequencing. Recent studies of additional data types, including methylation, DNase I hypersensitive sites, and single-cell ATAC-seq, have corroborated the existence of A/B compartments as functional units of genome organization. The genome can be further subdivided into sub-compartments, where genomic regions within a given sub-compartment are more likely to interact with each other than with regions in different sub-compartments. Subsequent to the A/B compartment model, a three-sub-compartment model was introduced based on higher-resolution Hi-C inter-chromosomal interaction data: one sub-compartment is a component of the open chromatin compartment; and the other two sub-compartments are components of closed chromatin compartment, one near centromeres and the other far from centromeres. The latest model proposes five sub-compartments based on the use of hidden Markov modeling (HMM) to cluster inter-chromosomal interactions. This method identifies two active sub-compartments (A1 and A2) and three inactive sub-compartments (B1, B2, and B3) using deeply sequenced GM12878 cell line data. The model also shows that the five sub-compartments exhibit distinct epigenetic signatures. Since sub-compartments are essential for understanding higher-order 3D genome organization, and an increasing volume of genome-wide chromatin interaction data will soon be available through the ENCODE and 4D Nucleome consortia, there is a practical need for an easy-to-use, automated, and accurate sub-compartment predictor.

In addition to Hi-C, other types of genome-wide sequencing data have been used to predict the higher-order genome organization. For example, chromatin immunoprecipitation sequencing (ChIP-seq) data of 11 histone modifications and 73 transcription factors (TFs) have been used to predict sub-compartments with 63% test accuracy using a deep learning multi-class classifier. Recently, TSA-Seq, a new genome-wide mapping method that estimates mean distances of chromosomal loci from nuclear structures, was used to predict several Mbp chromosome trajectories between nuclear structures. These findings use sub-compartment assignments either for predictive model output labels or for evaluation of the distances between nuclear speckles. These studies require accurate sub-compartment determination. Also, a DNA methylation correlation matrix based on multiple replicates corroborates the A/B compartment model. However, the potential of DNA methylation levels to predict nuclear sub-compartamentalization is still not clear.

Here, we introduce SCI, an algorithmic framework based on graph embedding and k-means clustering that predicts genomic sub-compartments from Hi-C data. We show that sub-compartment prediction by SCI is more accurate than other unsupervised algorithms. Furthermore, we use orthogonal data for external validation, including ChiP-PET chromatin interaction, transcriptome, and epigenome data. Lastly, using SCI output, we developed an epigenome-based (DNA methylation and histone modification) deep neural network model for sub-compartment classification.

Results

SCI overview. To predict sub-compartments, SCI starts with a normalized, genome-wide Hi-C inter-chromosomal contact matrix and constructs a Hi-C interaction graph, where each node on the graph represents a genomic bin. If two bins are interacting, an edge connecting them is added to the graph, and the weight of the edge corresponds to the normalized Hi-C sequencing read count between the two bins. Then, SCI uses graph embedding to project the interaction graph into a lower-dimensional vector space for k-means clustering to predict sub-compartments (Fig. 1a).

Specifically, SCI adapts a graph-embedding method termed LINE to project an otherwise high-dimensional graph structure into a lower-dimensional space that describes the chromatin interactions. LINE utilizes first-order and second-order proximities of graph vertices to reduce dimensionality and promote efficient clustering.

The number of sub-compartments in the nucleus is jointly determined by (a) the spatial location of chromatin and (b) chromatin interactions. Importantly, local epigenetic status can impact chromatin interactions. Using gap statistics to determine the optimal number of sub-compartments, we obtained nine as the optimal number of sub-compartments (named C1–C9). However, some of these sub-compartments are enriched for similar epigenetic modifications (C3 and C4; C5 and C6), suggesting that sub-compartments can be spatially separated and functionally comparable—they still show comparable levels of transcriptional potential (Supplementary Fig. 1). To allow for direct comparison of SCI with other computational methods for predicting sub-compartments, we chose to use 5 clusters in subsequent SCI performance evaluations. Importantly, SCI offers users the flexibility to select the number of sub-compartments based on either their preference or the optimal number calculated by gap statistics.

We then assessed the performance of SCI based on structural and functional evaluations (Fig. 1b). We also developed a deep neural network classifier for predicting sub-compartments using DNA sequencing data and epigenomic profiles (Fig. 1b).

SCI outperforms alternative algorithms. We compared sub-compartments predicted by SCI to those predicted by HMM (reported in Rao et al. 2014) and by k-means clustering applied directly to an inter-chromosomal interaction matrix (kmmeans_Yaffe, reported in Yaffe, E. and Tanay, A., 2011). We tested each algorithm using data from Rao et al., who generated 4.9 billion Hi-C reads from GM12878, a human lymphoblastoid ENCODE cell line.

When given the same parameter (k = 5), SCI predicted comparable number of sub-compartments as that predicted by HMM (C1–C5; Fig. 1c, Supplementary Fig. 3); however, kmmeans_Yaffe failed to predict five sub-compartments, as it placed genomic bins in four sub-compartments instead of 5 (Supplementary Fig. 2). Following the convention of Rao et al., we reordered sub-compartments predicted by SCI such that sub-compartments C1 and C2 correspond to open chromatin sub-compartments reported by Rao et al. (A1 and A2), while sub-compartments C3, C4, and C5 correspond to closed chromatin sub-compartments reported by Rao et al. (B1, B2, and B3). Sub-compartments C1 and C2 have higher gene density compared to the other three sub-compartments (Fig. 1d), which is consistent with the previous reports.

Our UMAP visualization of SCI embedding (Fig. 1e) shows: (i) a clear distinction between sub-compartments C1 (in red) and C2 (in yellow), which was indirectly reported in the literature by measuring the distance from lamina-associated domains (LADs); and (ii), clear separation of the inactive sub-compartment C3 (in gray) from the inactive sub-compartments C4 (in purple) and C5 (in blue). We further showed that the open...
Fig. 1 SCI utilizes a chromatin interaction graph to predict genomic sub-compartments. a The SCI workflow starts with a normalized Hi-C inter-chromosome matrix. From this matrix, the interaction graph is constructed; nodes with the same color represent bins from the same chromosome. After building the interaction graph, the graph embedding step transforms the graph into a lower-dimensional space. Finally, k-means clustering is used to cluster node representations. b SCI-predicted sub-compartments are validated using structural and functional properties and serve as class labels to train a sub-compartment classifier based on a feature matrix compiled with features of DNA sequence and epigenomic profiles (methylation and histone modifications), and replication timing data. c Bar plot of genomic bin count for each sub-compartment. d Bar plot of gene density measured as the number of genes per genomic bin for each sub-compartment. Sub-compartments associated with open chromatin (C1 and C2) show higher gene density compared to sub-compartments associated with closed chromatin (C3-C5). e UMAP 2-D projection of SCI’s embedding with 100 dimensions showing clustered sub-compartments for GM12878 Hi-C data. f ATAC-seq enrichment evaluating open and closed chromatin states across all five sub-compartments. g Distribution of nucleolar-associating domains (NADs) between C4 and C5. h–k Comparison of clustering quality metrics between SCI and HMM: (h) closeness centrality, (i) betweenness centrality, (j) clustering coefficient and (k) Silhouette index. For the boxplots, the top and bottom lines of each box represent the 75th and 25th percentiles of the samples, respectively. The line inside each box represents the median of the samples. The upper and lower lines above and below the boxes are the whiskers. Asterisks (***) represent p-values < 2.2e−16 using Mann-Whitney test.
chromatin-associated sub-compartments (C1 and C2) have higher enrichment of ATAC-seq compared to the inactive compartments (Fig. 1f, open-chromatin sub-compartment C1 compared to closed-chromatin sub-compartment C3, and open-chromatin sub-compartment C2 compared to closed-chromatin sub-compartment C5). Moreover, we show that C4 is more highly enriched for nucleolar-associating chromosomal domains (NADs) compared to C5 (Fig. 1g), indicating that C4 is located in the nucleolus while C5 is likely not. Thus, SCI-predicted sub-compartments exhibit distinct chromatin characteristics.

Genomic regions that map to the same sub-compartment based on the graph embedding of SCI are expected to be in proximity to each other in 3D space. To test this, we examined intra-sub-compartment, inter-chromosomal chromatin interaction network topology features, including network centrality (closeness and betweenness) and the clustering coefficient. Compared to the HMM approach, SCI showed significantly higher closeness centrality ($p < 2.2 \times 10^{-16}$, Mann-Whitney test) and betweenness centrality, and a higher graph clustering coefficient within sub-compartments (Fig. 1h–i), with improvements between 8–10%. In addition, we found that open sub-compartments (C1 and C2) show higher centrality values for chromatin interactions compared to the closed sub-compartments (C3, C4, C5) (Supplementary Fig. 3), indicating that heterochromatin is more spatially constrained than euchromatin. These topological network features indicate higher chromatin interactions between genomic regions within the same SCI-predicted sub-compartments. To further evaluate the clustering performance of SCI and HMM, we calculated their Silhouette coefficients. These topological network features indicate higher chromatin interactions between genomic regions within the same SCI-predicted sub-compartments. To further evaluate the clustering performance of SCI and HMM, we calculated their Silhouette coefficients, which measure the consistency within clusters of data.

The Silhouette index ranges from −1 to 1, where a higher value indicates better clustering performance. SCI improved the Silhouette index over the previous HMM sub-compartment annotation by 8% (Fig. 1k). Moreover, we calculated the Davies-Bouldin index, where lower values are better, and SCI improved the Davies-Bouldin index by 7% (Supplementary Fig. 4). We also compared LINE to the state-of-the-art graph embedding algorithms HOPE and DeepWalk. LINE-based cluster results had a better Silhouette index and centrality measures compared to the alternative graph embedding methods (Supplementary Fig. 5).

**Functional assessment of sub-compartments.** To compare the functional properties of sub-compartments predicted by SCI with those of sub-compartments predicted by other methods, we assessed enrichment for epigenomic marks and replication timing within sub-compartments. Data comprising DNase hypersensitive sites (DHS) (open chromatin), ten histone modifications, enhancer annotations, super-enhancer annotations, DNA methylation, and six replication timing datasets (Fig. 3a, Supplementary Fig. 7). We observed higher enrichment for enhancers and super-enhancers in the C1 and C2 sub-compartments predicted by both SCI and HMM (Fig. 3a, Supplementary Fig. 7), consistent with transcriptionally active genomic regions.

Genes in close 3D spatial proximity to one another are more likely to have synchronized transcriptional control compared to those that are in different sub-compartments. Therefore, we examined transcriptional activity in SCI-predicted sub-compartments. We assessed gene-expression levels using ENCODE RNA-seq data of GM12878 cells. Genes within C1 and C2 had significantly higher transcript per million (TPM) values ($p < 0.01$ based on ANOVA) compared to genes within C3-5, consistent with their epigenetic regulatory status (Fig. 3b). Furthermore, we evaluated the generation of nascent RNA using Global run-on sequencing (GRO-seq). The GRO-seq data confirmed that transcriptional activity in C1 and C2 is significantly higher (fold change $> 3$, $p < 0.01$ based on ANOVA) than that in sub-compartments C3-5 (Fig. 3c).

We hypothesize that the expression of genes within the same sub-compartment is more highly coordinated than that of genes across different sub-compartments. Therefore, we calculated pairwise Spearman’s correlation of gene expression for gene pairs within the same sub-compartment and across sub-compartments. We observed higher pairwise correlation values of gene expression for genes falling into bins within the same sub-compartment (intra-compartment correlation) compared to genes in different sub-compartments (inter-compartment correlation) (Fig. 3d). We also showed that SCI achieved a significantly higher ($P$-value $< 2.2e−16$, paired Wilcoxon test) intra-compartment correlation to the inter-compartment correlation ratio compared to HMM. As shown in Fig. 3e, SCI performs 40% better than HMM with respect to pairwise gene-expression correlation for functional evaluation of sub-compartments.
Folding the genome into sub-compartments may optimize the efficient usage of transcriptional regulatory elements. If true, we would expect to see sub-compartment-specific TF enrichment. To test this, we assessed TF enrichment using elastic net regression, which infers the regulatory elements that control transcription for each sub-compartment. Based on feature dependency analysis (see Methods section for details), we identified sub-compartment-specific TFs that can be used to predict gene-expression levels in each sub-compartment (Supplementary Table 1). We also identified sub-compartment-specific TFs (red text in Fig. 4a, b). To further validate C1- and C2-specific TFs, we evaluated ENCODE ChIP-seq data that was available for MYC, EP300, and BRCA1 TFs. We found that ChIP-seq-based TF enrichment patterns agree with the predicted sub-compartment-specific TFs, where MYC and BRCA1 are enriched in C1, and BATF and EP300 are enriched in C2 (Fig. 4c). In addition, we observed that YY1, a TF common to both C1 and C2, is not enriched in either sub-compartment. These results indicate that SCI can identify chromatin hierarchical sub-compartments that parse into transcriptional regulatory units.

Deep neural network for predicting sub-compartments. Recently, models have been proposed for predicting sub-compartment-level

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**Fig. 2 External validation of SCI-predicted sub-compartments using orthogonal ChIA-PET chromatin interaction data.** Validation using CTCF ChIA-PET (a-c) and RNAPII ChIA-PET (d-f). a, d Heatmaps of ChIA-PET loop counts per predicted sub-compartment, based on the mapping of loop anchors to genomic bins. Loop counts normalized genome-wide using sub-compartments determined by SCI. b, e Bar plots comparing the ratios of ChIA-PET loops connecting genomic bins within the same sub-compartment to the loops connecting genomic bins from different sub-compartments, based on the sub-compartment predictions by SCI and HMM. g Example regions of SCI sub-compartment predictions that have more intra-sub-compartment loops (intra-loops) than inter-sub-compartment loops (inter-loops) supported by CTCF and RNAPII ChIA-PET. Asterisks (***') represent p-value < 2.2 × 10⁻¹⁶ using Fisher's exact test.
Fig. 3 SCI sub-compartment have distinct genomic features. a Heatmap of distinct epigenomic sub-compartment predicted by SCI. b Boxplot of gene expression in transcripts per million (TPM) for different compartments. C1 and C2 have higher gene expression compared to other sub-compartment. c Spearman’s correlation coefficient ratio (y-axis) of gene pairs within the same sub-compartment (in black) vs. gene pairs across sub-compartment (gray) within 10 Mbps. d Spearman correlation vs. distance between gene pairs within the same sub-compartment (in black) vs. gene pairs across sub-compartment (gray) within 10 Mbps. e Ratio = Intra-sub-compartment ρ/Inter-sub-compartment ρ.

Fig. 4 Sub-compartment-specific transcription factor prediction. a-b Scatter plot showing sub-compartment-specific transcription factors (TFs) participating in transcriptional regulation predicted by elastic net regression for C1 and C2 sub-compartment. The star indicates TFs with the ChIP-seq data available from ENCODE (red: C1-specific regulators, orange: C2-specific regulator, and gray: shared regulator). c Heatmap of ChIP-seq enrichment for MYC, BRCA1, BATF, EP300, and YY1 TFs across sub-compartment.

The latter of which is a measurement of epigenome stochasticity21 (Fig. 5a). Building on these distinctions, we developed an epigenome-based classifier to predict sub-compartment based on ChIP-seq epigenomic marks and whole-genome bisulfite sequencing data, using a deep neural network (DNN) (Fig. 5b). We combined dynamic epigenomic features and static DNA sequence features to design a deep neural network (DNN). We sliced the data set into a training set (80%) and test set (20%). The model accuracy reached higher test accuracy (0.73) using SCI-detectected class labels than using HMM-detected class labels (0.68) or using randomized class labels (0.23) with the same class sizes.
developed model using 84 ChIP-seq libraries for histone modifications. The XGBoost and random forest methods agreed that histone modifications followed by DNA methylation distribution and replication timing data were significant predictors of sub-compartment prediction using random classifier trained with random labels, HMM sub-compartment annotation, or SCI sub-compartment annotation.

(Fig. 5c). In addition, we developed a more compact model using only DNA methylation and DNA based features, which was able to predict genomic sub-compartments with 0.66 of accuracy. Because the model interpretability of DNN is limited, we used a gradient-boosted trees model (XGBoost) classifier and random forest machine learning methods to derive a feature importance score for our features. The accuracy of the XGBoost classifier is 0.69, and the accuracy of the random forest method is 0.67, each of which is slightly lower than the accuracy of our DNN model. The XGBoost and random forest methods agreed that histone modification features followed by DNA methylation distribution are the most important feature in the dataset (Supplementary Fig. 8).

Our sub-compartment DNN predictors outperformed recently developed models using 84 ChIP-seq libraries for histone modifications and TFs using the same training/test data split (training data is from odd-numbered chromosomes and test data is from even-numbered chromosomes) (Supplementary Table 2). Moreover, our reduced model using DNA methylation and DNA features outperformed their reduced model using 11 histone marks.

**Compartment prediction using Hi-C or ChIA-PET data.** We also used SCI to predict A/B compartments from Hi-C and ChIA-PET data on two cell lines: GM128787 (human B-lymphocyte) and K562 (human lymphoblast). We predicted A/B compartments using a 100-kb resolution. We observed high agreement for A/B compartment prediction from both technologies (Supplementary Fig. 9) (agreement for GM12878 is 91% and agreement for K562 is 78%). We observed high correlation (0.88 for GM12878 and 0.76 for K562) for the first eigenvector values between Hi-C and ChIA-PET. Moreover, we noted that enrichment for several open chromatin marks, histone marks, and replication timing data was similar using compartments called by Hi-C and ChIA-PET for both cell lines (Supplementary Fig. 10). We implemented the compartment predictor using static features (DNA sequence information) and dynamic features (DNA methylation information) as input for the deep neural network model and achieved 87% test accuracy (Supplementary Fig. 11).

**Discussion**

Hi-C enables the elucidation of higher-order chromatin topology that suggests structural regulation of transcriptional control. Software exists for data pre-processing, chromatin loop calling, and topologically associating domain (TAD) predictions. However, there is no available software to examine compartment and sub-compartment structures. Furthermore, it has been shown that the TAD structure is rather stable among different cell types, while the structure of sub-compartments is highly variable among different cell types; this validates the need to study the cell type-specific functions of sub-compartments. SCI identifies complex nuclear sub-compartments in a fully data-driven, unsupervised fashion.

In contrast to previous methods that infer sub-compartments using HMM, SCI more comprehensively utilizes network properties and thus may preserve the global structure of the chromatin interaction network. SCI formulates sub-compartment prediction as a graph-based problem and enables efficient utilization of Hi-C information via graph embedding. SCI considers both the first-order and second-order proximities, which complement the sparsity of first-order proximity in Hi-C data. We demonstrated that SCI outperforms other algorithms, such as HMM and Kmeans_Yaffe. We believe that the superior performance of SCI compared to other methods is due to its use of all the inter-chromosomal interactions, and efficient dimensionality reduction via graph embedding. Specifically, Rao_HMM uses only a subset of inter-chromosome interactions, and Kmeans_Yaffe does not perform a dimensionality reduction on the data. Importantly, we studied the functional relevance of sub-compartments as they relate to cellular processes. Moreover, we show TF enrichment in SCI-predicted sub-compartments.

Recently, various computational models have been proposed to predict genome organization from sequence and epigenomic data and other 3D genome assays. We believe that SCI will further propel the development of such models by providing robust, accurate labels for genomic sub-compartments. As an example, we developed compartment and sub-compartment DNN predictors using static features from the DNA sequence of the reference genome and dynamic features from histone modifications and DNA methylation data and outperformed the other methods.
published model using 84 ENCODE ChIP-seq libraries for histone modifications and TFs from the same cell line.

Importantly, the ENCODE and 4D Nucleosome consortia are generating robust Hi-C datasets, and we anticipate that SCI will contribute to more efficient and accurate sub-compartment determination, and will improve our understanding of the complex interactions between DNA methylation, gene expression, and chromatin organization. Furthermore, tens of thousands of DNA methylation assays have been generated in large-scale studies such as The Cancer Genome Atlas, the Epigenome Roadmap, and Cancer Cell Line Encyclopedia. SCI will provide methods to maximize the value of these datasets and thereby enrich our understanding of the layers of gene-expression coordination that are important for development and disease states.

**Methods**

**Background.** All current sub-compartment prediction methods utilize an inter-chromosomal interaction matrix to predict sub-compartments. Two models for prediction of genomic sub-compartments have been published. First model is the Yaffe and Tanay sub-compartment model (Yaffe_Kmeans). This model applies K-means clustering directly to a HiC interaction matrix. It modifies the distance calculation method such that it ignores all distance computation that involves intra-chromosomes entries. This model identiﬁed three sub-compartments: one active and two inactive sub-compartments. The second model is Rao sub-compartments (HMM). The Rao sub-compartment prediction method focuses on one sub-set of inter-chromosomal interactions: the interactions between odd-numbered and even-numbered chromosomes. This method uses HMM to cluster the interactions between odd-numbered and even-numbered chromosomes in different runs. After performing cluster annotation for odd-numbered and even-numbered chromosomes, the Rao method combines those annotations into a single final cluster annotation based on enriched HiC interactions between the clusters of odd-numbered and even-numbered chromosomes.

**Graph-embedding methods.** Given an undirected graph $G = [V, E]$, where $V$ represents genomic bins, and $E$ represents Hi-C interactions, each edge $(e)$ between $v_i$ and $v_j$ has weight $w_{ij}$, which represents the normalized Hi-C read count. Graph-embedding approaches project graph $G$ into a low dimension space Rd by calculating embedding matrix $U$ (please refer to the following reviews for more detailed information about graph embedding)[1–3]. We compared SCI graph embedding method to DeepWalk and HOPE graph embedding methods.

The Deepwalk method relies on performing random walks across the graph that have a specific length. These walks resemble node sequences in the graph, and this sequence is led to the Word2Vec approach to derive the embedding of the graph vertices based on their context. The original DeepWalk implementation handles only unweighted graphs. We used a modified version of the algorithm to handle weighted graphs from (https://github.com/dongquosheng/deepwalk).

The HOPE method derives the graph embedding matrix $U$, which minimizes the following objective function:

$$\min \left[ \frac{1}{2} \sum_{i<j} \left( S_{ij} - u_i^T u_j \right)^2 \right]$$

where $S$ is a similarity matrix, and $U$ is an embedding matrix where $U = [u_1, u_2, \ldots, u_n]$. The similarity matrix can be defined using different similarity measures, including the Katz index and rooted page rank. For HOPE, we used the implementation of these algorithms from the GEM graph embedding package (https://github.com/palash1992/GEM). We used Katz index similarity measures in the original publication[41].

**LINE and joint optimization.** In order to project graph $G$ into lower dimension $R^d$, LINE defines two properties to preserve in the graph: first-order proximity and second-order proximity.

First-order proximity is defined as the pairwise proximity through edges between the vertices in graph $G$. LINE models first-order proximity between two vertices in graph $v_i$ and $v_j$:

$$p_1 = \frac{1}{1 + e^{-d_{ij}}}$$

where $u_i$ and $u_j$ are vertices embedding into low-dimensional space $R^d$. We define empirical edge distribution over the space $V \times V$, $p_1 = \frac{1}{W}$ where $W = \sum_{i \neq j} w_{ij}$. To obtain the first-order embedding, LINE optimizes the KL divergence (emitting constants) between $p_1$ and $p_1$ as:

$$O_1 = -\sum_{i \neq j} w_{ij} \log(p_1(v_i, v_j))$$

For second-order proximity, the main assumption is that vertices connected to other vertices are similar. To calculate embedding based on the second-order proximity, LINE introduces the concept context. Each vertex in the graph is considered as a simple vertex or as a context to other vertices. LINE introduces two vectors $u_i$ and $u'_i$, where $u_i$ is the representation for $v_i$ as a vertex while $u'_i$ is the representation for $v_i$ as a context.

For each directed edge in the graph $(i, j)$ (undirected edges are treated as two directed edges with opposite directions), LINE defines the probability of context $v_j$ generated by vertex $v_i$ as:

$$p_2(v_j|v_i) = \frac{\exp(u'_j - u_i)}{\sum_{v \in V} \exp(u'_v - u_i)}$$

Empirical distribution $p_2$ is defined as $p_2 = \frac{1}{d}$, where $d_k$ is the out-degree of node $i$. LINE optimizes scaled (by node degree) versions of the KL divergence between $p_2$ and $p_1$. It defines:

$$O_2 = -\sum_{w_{ij}} w_{ij} \log(p_2(v_j|v_i))$$

SCI implements two approaches to combine defined objective functions $O_1$ and $O_2$. In the first approach, SCI optimizes $O_1$ and $O_2$ independently and then combines representation from both orders into a final representation. In the second approach (joint optimization), SCI combines first-order and second-order proximity objective functions into one function to define $O_3$ as:

$$O_3 = (1 - \alpha)O_1 + \alpha O_2, \ \alpha \in [0, 1]$$

where $\alpha$ is a mixing parameter to determine the weight of first-order and second-order optimization functions.

It then optimizes both orders at the same time. An asynchronous gradient descent algorithm coupled with negative sampling is used to optimize all objective functions. The joint optimization showed a 30% increase in time efficiency (from 26 min to 18 min using GM12878 Hi-C data) and a slightly lower clustering performance of the joint optimization compared to separate optimization (measured by Silhouette index, Davies-Bouldin index, and centrality measures, Supplementary Fig. 12). Both separate and joint optimization are available as options in the SCI code.

**Evaluation for clustering methods.** For each genomic bin we define Silhouette index ($s_i$) as:

$$s_i = \frac{b_i - a_i}{\max(b_i, a_i)}$$

where $b_i$ is the lowest average distance for genomic bin $i$ for all other clusters, and $a_i$ is the average distance from genomic bin $i$ from all points in the same cluster.

We used the silhouette_score function from scikit-learn package version 0.19.2.

We used Euclidean distance as our distance measure.

The Davies–Bouldin index (DBI) is defined as:

$$DBI = \frac{1}{k} \sum_{i=1}^{k} \max_{j \neq i} \frac{D_{ij}}{D_{ii}}$$

where

$$D_{ij} = \frac{d_{ij} + d_{ji}}{2}$$

Following the definition in ref. 26, we define $d_{ij}$ and $d_{ji}$ as the average distance between all pairs in clusters $i$ and $j$. $D_{ij}$ is the distance between all pairs between clusters $i$ and $j$.

The clustering coefficient is defined as the ratio of the number of closed triplets (triangles) the node has to the number of all triplets that the node has. To adjust to the weighted graph, the weighted average for the closed triplets is calculated:

Closeness network centrality of a node is defined as the average length of the shortest path between the node and all other nodes in the graph. Closeness centrality for a node $u$ in a graph with $n$ nodes can be calculated as:

$$C(u) = \frac{n - 1}{\sum_{v \neq u} d(v, u)}$$

where $d(v, u)$ is the shortest path between nodes $v$ and $u$.

Betweenness network centrality is defined as the number of times a node acts as a bridge along the shortest path between two other nodes. Betweenness centrality for a node $u$ in a graph with $n$ nodes can be calculated as:

$$C_B = \sum_{s \neq t \neq u} \sigma(s, t | u)$$

where $V$ is the total number of nodes in the graph, $\sigma(s, t)$ is the number of shortest paths between nodes $s$ and $t$. $\sigma(s, t | u)$ is the number of shortest paths between $s$ and $t$ passing through $u$.

Closeness and betweenness centralities were calculated using NetworkX version 2.1.

GM12878 CTCF and RNAAPII ChIA-PET intra-chromosome loops supported by at least five paired-end reads were used for loop ratio calculation. A loop anchor is associated with a specific sub-compartment if it has an overlapping ratio greater
than 50%. Next, we create sub-compartment loop interaction matrix \( M(m_i,j) \), where \( m_i \) represents the number interaction between sub-compartments \( i \) and \( j \) detected using CHIA-PET data, such that the CHIA-PET loop left anchor falls in sub-compartment \( i \) and the right anchor falls in sub-compartment \( j \). As there is no directionality difference between the left and right anchors, we create a symmetric compartment matrix \( M_{sym} \) as the sum of \( M \) and \( M^T \). Finally, a normalized matrix \( (M_{norm}) \) is obtained by dividing \( M_{sym} \) by the sum of its all elements.

An inter-compartment loop was defined as a CHIA-PET loop with both anchors falling in genomic bins belonging to the same sub-compartment. Inter-sub-compartment loops were defined if two anchors of the loops fall in genomic bins from different sub-compartments. The ratio of the number of intra-sub-compartment and the number of inter-sub-compartment were then used to assess the connectivity of the predicted sub-compartments.

Sub-compartment and compartment prediction using epigenome data. We developed machine learning and deep learning models for sub-compartment and compartment predictions using DNA sequence static features and epigenomic anchors falling in genomic bins belonging to the same sub-compartment. Inter-compartment matrix directionality difference between the left and right anchors, we create a symmetric sub-compartment matrix. Finally, we performed feature dependency analysis across samples to determine regulators that significantly account for compartment-specific gene expression in the regression models.

Sub-compartment regulator inference. We obtained the DNA binding motifs of transcription factors (TFs) from the CIS-BP database. We mapped TFs to the hg19 sequences using FIMO32, and we retained TF hits with FDR < 0.1. Then, we associated TF binding sites (TFBS) with genes if the predicted TFBS were within 2 kb of a gene TSS. We further filtered TFBS by selecting only those in accessible chromatin regions, as determined by ATAC-seq data. Finally, we constructed a features matrix where the genes represent samples, and all mapped TFs represent features, and where the count of TF hits associated with a given gene reflects the feature value. We modified the RegulatorInference tool (https://bitbucket.org/leslielab/regulatorinference) to implement a sample-by-sample elastic net regression model to predict gene expression for each replicate using regulatory elements in gene promoters. We optimized the elastic net mixing parameter (alpha) using ten fold cross-validation. Based on the minimum squared error (mse), we picked an alpha value of 0.3 (Supplementary Fig. 13).

As a result of elastic net regression, we obtained a coefficient vector for TFs that represents the importance of the corresponding TF for the prediction of gene expression, while the sign of the coefficient can be interpreted as the predicted direction of regulation. We performed elastic net regression tasks separately for each sub-compartment.

Finally, we performed feature dependency analysis across samples to determine regulators that significantly account for compartment-specific gene expression in the regression models. In this process, the aggregate error change of one TF was calculated. In summary, the aggregate error corresponds to the difference between the total regression error and the error contributed by a specific TF across the six different RNA-seq datasets used. To calculate the aggregate error for each elastic net model, initially, the entire error is measured using all learned TF coefficients. Then the TF coefficients are set to zero one at a time, the error contributed by a specific TF is calculated. Lastly, the difference between both errors is calculated for each model and aggregated over the different models to define the final aggregate error. The higher the aggregate error value, the most important the TF. If the aggregate error change of a TF is higher than the cutoff, it is considered an important TF. We used the default RegulatorInference tool cutoff, which corresponds to the mean of aggregate error changes across all TFs plus 1.5 times the standard deviation of aggregate error changes across all TFs.

Epigenomic signal enrichment. The enrichment of the epigenomic signal was calculated based on the description of (Rao et al., 2014). Briefly, to calculate enrichment for epigenomic data, we used bwtool36 to calculate the mean of the normalized signal for each histone mark in each bin downloaded from the ENCODE consortium data portal (see data availability). Then, we computed enrichment as the ratio of the median of ChIP-seq signal for all of the bins in each sub-compartment divided by the median of ChIP-seq signal of all of the bins genome-wide.

Transcription factors enrichment. We obtained all ENCODE uniformly processed peaks from (http://hgdownload.cse.ucsc.edu/goldenPath/hg19/encodeDCC wgEncodeAwgFbsUniform/). We assigned peaks to different sub-compartments using bedtools37. We calculated peak enrichment in specific sub-compartments as the average peak abundance in a specific sub-compartment divided by genome-wide peak abundance. We evaluated the significance of the presence of a specific TF in a sub-compartment using the Mann-Whitney test compared to the genome-wide background. We considered only those TFs with corrected p-value < 0.05 in at least one compartment. To evaluate the significance between C1 and C2 sub-compartments, we used a two-tailed Mann-Whitney test.

Pairwise correlation among genomic bins using RNA-seq. Correlation of gene-expression levels within the same or different compartments was computed only for those genes expressed in at least one of the studied replicates. Each gene was represented as one TSS, corresponding to the 5’ end of the “gene” feature from Gencode. We used the correlation coefficient to compute the correlation of gene-expression levels within the same or different compartments. Finally, the average value of Spearman’s correlation coefficients was computed for all intra-compartment and inter-compartment pairs, considering only those for which results were statistically significant (i.e., p-value < 0.05). All of the above-described steps were conducted for the maximum range between pairs up to 10 Mb with a 100 Kb step.

Gene-expression levels comparison using RNA-seq. We used transcript-per-megabase (TPM) values from RNA-seq transcript quantification to obtain the gene level in the box of Fig. 3b. We assigned gene TSSs to different sub-compartments, and then we plotted a boxplot using seaborn package version 0.9.0.

Transcription efficiency measured by GRO-seq. We used bwtool to extract an aggregation plot36 for GRO-seq data around each TSS for each sub-compartment separately.

DNA methylation data preprocessing. Briefly, whole genome bisulfite sequencing (WGBS) data were first trimmed of adapters using Trimm_galore (version 0.4.0) [http://github.com/lundquistlaboratory/trim_galore/]. The base quality of the trimmed reads was checked with FastQC (version 0.11.5) [http://www.bioinformatics.babraham.ac.uk/projects/fastqc/]. The preprocessed reads were then
aligned to human genome reference hg19 using Bismark (version 0.16.1)37. The aligned reads were then deduplicated, and the methylation call at each CpG site was determined by running the appropriate Bismark scripts. DNA methylation patterns were calculated using methcne38; epipolyomorphism39 and PDR21 were calculated using epiphet (https://www.biocor堕tor.org/packages/devel/bioc/html/epiphet.html).

**ATAC-seq data processing.** We used HMCan40 to obtain signal tracks from the alignment data.

**Enhancer and super-enhancers enrichment.** We calculated enhancer and super-enhancer enrichment as the ratio between the expected value of observing a super-enhancer (or enhancer) per compartment and the expected value of observing a super-enhancer (or enhancer) genome-wide.

**Reporting summary.** Further information on research design is available in the Nature Research Reporting Summary linked to this article.

**Data availability**

We obtained processed (big) formatted Hi-C data for both GM12878 and K562 cell-lines from5 with GEO entry GSE63525, GM12878 CHIA-PET data accession code of 4D Nucleosome consortium (https://commonfund.nih.gov/4dnucleome) is 4DNES71559L9 (CTCF) and 4DNESZ225MOZV (RNAPII). We obtained raw CHIA-PET for CTCF and RNAPII factor for K562 cell-line from ENCODE. We processed raw files to produce tracks follow the Links: https://www.encodeproject.org/experiments/ENCST800B7VZ and https://www.encodeproject.org/experiments/ENCST800CAC1I. We used ATAC-seq data generated by41 GEO entry GSE67753. We downloaded signal bigwig tracks for DHS and histone modifications from the ENCODE consortium using the following link: http://gtr.ebi.ac.uk/pub/databases/ensemble/integration_data_jan2011/byDataType/signal/. We obtained NAD enriched regions published in12 generated by41 GEO entry GSE47753. We downloaded signal bigwig tracks for DHS and histone modifications from the ENCODE consortium using the following link: http://gtr.eari.ac.uk/pub/databases/ensemble/integration_data_jan2011/byDataType/signal/. We obtained raw ChIA-PET for CTCF and from DENdb enhancers database43 (https://www.cbrc.kaust.edu.sa/dendb/), and used GEO accessions: GSE88583, GSE88627, GSM958730, GSE90222, GSE78553, GSE78555.

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Author contributions
S.L. conceived the project, H.A. and S.L. designed the algorithm and deep neural network architecture, and H.A. implemented the algorithms, developed software, and performed computational analysis. X.C., W.R., J.W., P.W., Y.R., and S.L. contributed to analysis of SCI evaluation. H.A., A.C., and S.L. contribute to the revision. H.A. and S.L. wrote the paper.

Competing interests
The authors declare no competing interests.

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