Environmental dependence of X-ray and optical properties of galaxy clusters

Citation for published version:
Manolopoulou, M, Hoyle, B, Mann, RG, Sahlen, M & Nadathur, S 2021, 'Environmental dependence of X-ray and optical properties of galaxy clusters', Monthly Notices of the Royal Astronomical Society, vol. 500, no. 2, pp. 1953-1963. https://doi.org/10.1093/mnras/staa3341

Digital Object Identifier (DOI):
10.1093/mnras/staa3341

Link:
Link to publication record in Edinburgh Research Explorer

Document Version:
Peer reviewed version

Published In:
Monthly Notices of the Royal Astronomical Society

General rights
Copyright for the publications made accessible via the Edinburgh Research Explorer is retained by the author(s) and / or other copyright owners and it is a condition of accessing these publications that users recognise and abide by the legal requirements associated with these rights.

Take down policy
The University of Edinburgh has made every reasonable effort to ensure that Edinburgh Research Explorer content complies with UK legislation. If you believe that the public display of this file breaches copyright please contact openaccess@ed.ac.uk providing details, and we will remove access to the work immediately and investigate your claim.
Environmental dependence of X-ray and optical properties of galaxy clusters

M. Manolopoulou1⋆, B. Hoyle2, R. G. Mann1, M. Sahlén3 and S. Nadathur4

1 Institute for Astronomy, University of Edinburgh, Blackford Hill, EH9 3HJ, Edinburgh, UK
2 Universitaets-Sternwarte, Fakultät für Physik, Ludwig-Maximilians Universität München, Scheinerstr. 1, D-81679 München, Germany
3 Department of Physics and Astronomy, Uppsala University, Box 516, SE-75120 Uppsala, Sweden
4 Institute of Cosmology and Gravitation, University of Portsmouth, Burnaby Road, Portsmouth, PO1 3FX, UK

Accepted 2020 October 21. Received 2020 October 21; in original form 2020 March 10

ABSTRACT

Galaxy clusters are widely used to constrain cosmological parameters through their properties, such as masses, luminosity and temperature distributions. One should take into account all kinds of biases that could affect these analyses in order to obtain reliable constraints. In this work, we study the difference in the properties of clusters residing in different large scale environments, defined by their position within or outside of voids, and the density of their surrounding space. We use both observational and simulation cluster and void catalogues, i.e. XCS and redMaPPer clusters, BOSS voids, and Magneticum simulations. We devise two different environmental proxies for the clusters and study their redshift, richness, mass, X-ray luminosity and temperature distributions as well as some properties of their galaxy populations. We use the Kolmogorov-Smirnov two-sample test to discover that richer and more massive clusters are more prevalent in overdense regions and outside of voids. We also find that clusters of matched richness and mass in overdense regions and outside voids tend to have higher X-ray luminosities and temperatures. These differences could have important implications for precision cosmology with clusters of galaxies, since cluster mass calibrations can vary with environment.

Key words: galaxies: clusters: general – cosmology: large-scale structure of Universe – X-rays: galaxies: clusters

1 INTRODUCTION

The large-scale structure of the Universe resembles a cosmic web, the density of which is traced by millions of observed galaxies. These galaxies themselves also collapse into galaxy groups and galaxy clusters, which are often located along the walls and filaments of the Cosmic Web. Knots are the intersection of filaments at which point collections of galaxy superclusters are found (for a review see Springel et al. 2006). The rest of the space in the Cosmic Web is underdense compared to the walls, filaments and knots, but not devoid of galaxies, and occasionally even galaxy groups and galaxy clusters. These underdense regions are known as voids.

 Differences in the properties of the galaxy populations in these different large scale structure environments have been found. Dressler (1980) examined the relationship between local density and galaxy morphology and found indications of increasing elliptical and S0 population and a corresponding decreasing spiral population with increasing density as well as a trend of increasing luminosity of the spheroidal component of galaxies with increasing local density. Additionally, Meneux et al. (2006) concluded that luminous late-type galaxies are located in more clustered, higher-density regions than are less luminous galaxies. In Ricciardelli et al. (2017), the authors showed that galaxies which inhabit voids have later galaxy-type morphologies at all stellar masses and that the later-type galaxies appear at smaller distances from the void centre than early-type galaxies. Darvish et al. (2018) concluded that the molecular gas content and the subsequent star-formation activity of star-forming and starburst galaxies are not affected by their local environment since $z \approx 3.5$. In Wang et al. (2018), the main sequence of central galaxies and the fraction of star-forming galaxies were found to have no significant dependence on halo mass, while for satellite galaxies the position of the main sequence was found to be almost always lower compared to that of the field and the width is almost always

⋆ E-mail: mmanolop89@gmail.com

© 2020 The Authors
larger. The fraction of star-forming galaxies was seen to decrease with increasing halo mass and this dependence was found stronger towards lower redshift. Hoyle et al. (2012) found that void galaxies have bluer colours than galaxies in higher density environments with the same magnitude distribution; also an alignment of the disk galaxies angular momenta with the void’s radial direction was found in Varela et al. (2012).

Despite the small numbers of galaxies in voids and the typically large void volumes, galaxies still gravitationally attract each other to form groups and clusters of galaxies. The latter are expected to have fewer members and, therefore, smaller sizes and masses and to have undergone fewer mergers in their formation history with respect to the “field” clusters, which we define here as groups and clusters not inhabiting voids. As a result of the latter, there would be more relaxed clusters in number within voids than outside voids. Cautun et al. (2014) used cosmological simulations to find that voids and sheets are devoid of massive clusters. After classifying morphologically the Cosmic Web, Aragón-Calvo et al. (2010) promoted the idea that more massive clusters reside in areas of higher density, while less massive clusters reside in underdense regions. A study of the environmental dependence on the properties of galaxy groups occurred in Poudel et al. (2016) who found that groups in high-density environments show more efficient galaxy formation and higher abundances of satellite galaxies. Liao & Gao (2019) used hydrodynamical simulations to show that dark matter halos in filaments have higher baryon and stellar fractions than the field counterparts. Any difference in the properties of the clusters in different environmental densities would result in complex and currently unaccounted for selection effects. This would affect studies of galaxy groups and clusters; for example, it could potentially affect the currently adopted scaling relations between cluster observables and cluster masses, the calculation of the cluster power spectrum, which are crucial when using clusters to estimate cosmological parameters (e.g. Allen et al. 2011; Borgani 2008). The differences can be related to the recent conclusions of non-isotropy of the Universe due to spatial variation of the L-T cluster relations (Migkas et al. 2020). Some examples of the reasons why we expect to observe differences in the observed cluster properties as a function of local environment are possibly different merger rates of galaxies within the clusters, gravitational screening mechanisms which modify the force of gravity (e.g. Spiegel 1999) and changes to the cluster formation model (e.g. Kravtsov & Borgani 2012).

In this study, we search for differences in the X-ray and optical properties of galaxy clusters as a function of their environment using two methods. In the first we construct void catalogs from the galaxy positions and characterize clusters using this geometrical criterion, i.e. whether they reside inside voids or not. Secondly, we study the differences in cluster properties as a function of local density as directly estimated from the galaxy positions, without using void catalogues. We compare the redshift, richness, X-ray luminosity and temperature distributions of the clusters as well as the BCG and CMR fit properties of their galaxy populations. Some of these properties are widely used to infer the cluster mass: more massive clusters tend to have more galaxy members (i.e., are richer), and have higher temperatures and luminosities in their cores. Therefore, if differences were to be found in these properties between clusters in different large-scale environments, that would imply that an environmental bias correction should be introduced when inferring the cluster mass. Failure to do so could lead to systematically incorrect mass estimates. Since the cluster mass function is very steep, a relatively small systematic bias in the mass estimate could have a large impact on the expected cluster number density (Sahlen et al. 2009).

To model the large-scale environment we use a common set of voids derived from the Baryon Oscillation Spectroscopic Survey (BOSS, Dawson et al. 2013) spectroscopic galaxy catalogues, and both X-ray (XCS DR2-SDSS, Giles et al. 2020a) and optically selected (redMaPPer SDSS, Rykoff et al. 2014) cluster samples, which are presented in Section 2, together with a larger set of catalogues from Magneticum simulation data. In Section 3, we identify clusters within and outside voids and calculate the density of their environment. We describe our method of matching samples of different environments and comparing their properties. We then compare the cluster distributions of redshift, richness, mass, luminosity and temperature, brightest cluster galaxy (BCG) and colour-magnitude relation (CMR) fitting parameters within different local environments in Section 4. We create the mass functions of clusters within and outside voids and in overdense and underdense regions. We seek possible differences that would need to be accounted for when doing cosmological analyses using those cluster properties. We study the dependence of the cluster sample size on the results in Section 5. In Section 6, we present our main results and discuss the effect of the richness estimators in the difference of richness between clusters identified to reside within voids and not. We suggest future prospects of this project and, finally, conclude.

2 THE CATALOGUES

2.1 Observational data

2.1.1 Void catalogues

We use a catalogue of voids from the BOSS Data Release 12 galaxy catalogues (Alam et al. 2015), obtained using the REVOLVER void-finding algorithm (Nadathur et al. 2019). REVOLVER is derived from the earlier ZOBOV code (Neyrinck 2008). The algorithm reconstructs an estimate of the continuous galaxy density field from the discrete tracer distribution using Voronoi tessellations, and then identifies voids as corresponding to minima of this density field, with neighbouring voids delineated based on a watershed algorithm that makes no prior assumption about void shapes. REVOLVER accounts for the complex survey geometry using boundary buffer particles during tessellation, and includes additional corrections for the survey selection function and angular completeness using a weighting scheme described in detail in Nadathur & Hotchkiss (2014); Nadathur (2016); Nadathur et al. (2019).

Void catalogues for an earlier BOSS data release (DR11) were presented in Nadathur (2016). The DR12 versions of these catalogues used here have also previously been used

Available from https://github.com/seshnadathur/Revolver
in other studies, (e.g., Nadathur & Crittenden 2016; Kovács 2018; Nadathur et al. 2019; Raghunathan et al. 2019). The BOSS data consists of two distinct galaxy samples, LOWZ and CMASS, characterized by changes in the targeting, redshift range and sky coverage (Reid et al. 2016), and we apply REVOLVER separately to each. In order to achieve completeness of the void catalogues and avoid biasing our numbers of clusters found inside and outside voids, we apply further redshift cuts to obtain 2,968 voids in the redshift range of 0.16 ≤ z ≤ 0.41 from LOWZ, and 7,057 voids in 0.45 ≤ z ≤ 0.67 from CMASS. In total, these voids cover ∼ 80% of the total available survey volume (Nadathur 2016).

In the top panel of Figure 1 we present the initial BOSS CMASS and LOWZ redshift distributions in grey and the ones after the redshift cuts are applied, in blue and magenta respectively. In the bottom panel of Figure 1 we show the normalised distribution of the void effective radius in the two catalogues. CMASS voids have slightly larger sizes than LOWZ voids due to the lower mean galaxy number density, which reduces the spatial resolution of the voidfinder.

The void catalogues contain information about the void centre coordinates, the void effective radius (defined as the radius of a sphere of equivalent volume) and the minimum density within the voids. REVOLVER voids have peculiar 3-dimensional shapes (see Nadathur 2016 for an example illustration), making a representation of their shape by a sphere unrealistic. We instead model each void in the catalogue as an ellipsoid, and extract information on the lengths of the three ellipsoidal axes and their orientation with respect to the line of sight direction.

### 2.1.2 Cluster catalogues

We use a variety of cluster catalogues in order to explore both X-ray and optical properties of clusters in different environments. We use (i) the XMM Cluster Survey (XCS) Data Release 2–Sloan Digital Sky Survey catalogue (XCS DR2–SDSS, Giles et al. 2020a) to compare cluster X-ray luminosities and temperatures, (ii) the GMPhoRCC cluster catalogue, an X-ray selected cluster catalogue from XCS DR2 with optical properties extracted with the Gaussian Mixture full Photometric Red sequence Cluster Characteriser (GMPhoRCC, Hood & Mann 2017) and (iii) the redMaPPer SDSS DR8 catalogue (Rykoff et al. 2014) to take advantage of the large numbers of galaxy clusters with associated optical properties. We also use the Finoguenov et al. (2020) redMaPPer cluster subsample which contains clusters X-ray properties as an additional X-ray catalogue. The variation of the catalogue size enables us to study the effect of the sample size in our results.

The XCS DR2–SDSS catalogue is the XCS (Mehrtens et al. 2012) second data release of X-ray selected galaxy clusters within the SDSS area. The X-ray observations are collected from the XMM public archive and include all areas suitable for cluster searching as described in Lloyd-Davies et al. (2011). These result in 10,742 observations, each associated with an object ID, across the whole sky. The XCS analysis pipeline is described in detail in Section 2.3 of (Giles et al. 2020b), which creates an XCS master source list with associated classification of the source apparent size. The extended and Point Spread Function (PSF)-sized sources with number of X-ray soft band (0.5-2 keV) counts higher than 200 are subsequently optically confirmed as galaxy clusters using SDSS DR13 multi-band imaging and a Cluster-Zoo project\(^2\). Within the Cluster-Zoo project, members of the XCS collaboration individually eyeballed and confirmed or rejected the XMM sources as galaxy clusters. This process resulted into an X-ray selected, optically confirmed XCS galaxy cluster catalogue within the SDSS area, that contains 832 galaxy clusters in total. Section 2.5 of (Giles et al. 2020b) describes in detail the measurement of the X-ray properties, including the X-ray bolometric temperature and luminosity (core-included) in the 0.01 – 50 keV range of the clusters, which were measured within \(R_{500}\), the cluster radius where the density is 500 times higher than the critical density of the Universe. The cluster redshifts were measured using a variety of methods, giving priority to spectroscopic redshift when available. The spectroscopic redshifts were taken from \(\text{www.zooniverse.org}\) was used to host our Cluster-Zoo project.

\(^2\)
the literature (Rykoff et al. 2014) or were measured using the method of Hilton et al. (2018) with data from SDSS DR13 (Albareti et al. 2017), VIPERS PDR2 (Scocullo et al. 2018) and DEEP2 (Matthews et al. 2013). In the cases where we could not obtain spectroscopic redshift measurements, we measured photometric redshifts using primarily the GM-PhoRCC algorithm (Hood & Mann 2017) and the zCluster algorithm in the rest of the cases (Hilton et al. 2018). The final sample of 832 clusters spans a range of redshifts from 0.025 to 0.7475, with median of 0.286.

For a larger number of clusters and the availability of optical properties, we use an extension of the XCS DR2–SDSS catalogue, the GMPhoRCC catalogue. This contains 1,340 clusters with good quality GMPhoRCC flag, associated with optical properties such as red sequence redshift, richness, CMR fitting properties that are calculated with GMPhoRCC (Hood & Mann 2017) and X-ray luminosity and temperature calculated as for XCS DR2–SDSS clusters. These have not been optically confirmed through a cluster Zoo like the XCS DR2–SDSS sample or have the X-ray soft band counts threshold, a fact that increases the sample size in the same SDSS area compared to the XCS DR2–SDSS catalogue, but the lower quality of redshifts can contaminate it by including spurious X-ray cluster detections. However, X-ray detected clusters with good quality GMPhoRCC flag coincide with a galaxy overdensity on SDSS catalogue, a fact that optically confirms that they are clusters. This catalogue offers a wealth of optical properties to study: red sequence redshift, spectroscopic redshift, where available (coming from the galaxy members with available spectroscopic redshifts; these are usually 1-2 galaxies, but can be up to 5), red sequence colour, CMR width, CMR gradient, CMR intercept, richness within \( R_{200} \), BCG distance from the cluster centre (in arcminutes) and finally X-ray temperature within \( R_{500} \) and X-ray bolometric luminosity within \( R_{500} \) calculated using the same pipelines as the XCS DR2–SDSS catalogue.

The redMaPPer cluster catalogue is an optical catalogue which contains 396,047 galaxy clusters in the SDSS DR8 footprint created with the redMaPPer red sequence cluster finder (Rykoff et al. 2014). The catalogue contains the cluster redshift \( z_{\lambda} \), richness \( \lambda \), integrated luminosity in the \( i \)-band and BCG information (spectroscopic redshift, \( i \)-band magnitude and \( i \)-band luminosity). We use all six available properties in our analysis. As shown in (Rykoff et al. 2014), the catalogue completeness is richness dependent, therefore, apart from using the full catalogue, we also use the catalogue with extra cuts on the richness and/or redshift:

- **redMaPPer 1**: \( z \geq 0.3 \) and \( \lambda > 20 \),
- **redMaPPer 2**: full \( z \) range and \( \lambda > 20 \) and
- **redMaPPer 3**: full \( z \) range and \( \lambda > 30 \).

In Figure 2 all three redshift distributions of the cluster catalogues described above are presented. Additionally, we use a subsample of the redMaPPer cluster catalogue (Finoguenov et al. 2020) which contains the redMaPPer redshift and richness estimation and also the X-ray luminosity in the rest-frame 0.1-2.4\( keV \) and temperature in kHz. This catalogue contains 10,383 clusters and is used as an additional test for the environmental dependencies on X-ray cluster properties.

For more information refer to [http://magneticum.org/](http://magneticum.org/)

---

Figure 2. The normalised redshift distributions of the three cluster catalogues. In green, the redMaPPer clusters, in yellow, the XCS DR2–SDSS clusters and in red, the GMPhoRCC clusters.

### 2.2 Simulation data

In addition to the observational data, we use simulations to study the properties of large numbers of galaxy clusters inside and outside voids, without the effect of possible detection bias in our cluster and void populations. The Magneticum simulations (Hirschmann et al. 2014) are large-scale smoothed-particle hydrodynamic (SPH) simulations. They are based on the WMAP7 cosmology (Komatsu et al. 2011) and include a variety of physical processes, such as cooling, star formation and stellar winds, chemical enrichment, Active Galactic Nuclei (AGN) feedback and magnetic fields. For this study, we use the redshift \( z = 0.14 \) snapshot of the Box0 simulation, which has box side 2688 Mpc and \( 2 \times 4536^3 \) particles. This redshift is close to but somewhat smaller than that of the BOSS LOWZ data.

The cluster catalogue is created using a friends-of-friends algorithm with a linking length of 0.16 (Davis et al. 1985) that links only the dark matter particles. For each halo, the SUBFIND algorithm (Springel et al. 2001; Dolag et al. 2009) is run in parallel to compute the mass \( M \) of the cluster particles within the region where the density is 500 times the critical density of the Universe (Gupta et al. 2017). The centre of each cluster is assigned as its deepest gravitational potential position. The cluster temperature is the mean, mass-weighted temperature within \( R_{500} \) and the X-ray luminosity is calculated from the emissivity of every particle in the simulation following Bartelmann & Steinmetz (1996). For each cluster in the catalogue we have the mass \( M \) within \( R_{500} \), the temperature \( T_X \), and the bolometric X-Ray luminosity within \( R_{500} \), \( L_X \). The catalogue covers a large range of masses, from \( 10^{13}h^{-1}M_{\odot} \) to \( 10^{15}h^{-1}M_{\odot} \); however, we only use clusters with \( M > 10^{14}h^{-1}M_{\odot} \), where the extracted X-ray luminosities and temperatures are reliable (K. Dolag, private communication); this mass cut has also been used for Magneticum clusters in Gupta et al. (2017). This is a catalogue of \( \sim 105,000 \) simulated clusters, a much
larger X-ray cluster sample than XCS DR2–SDSS and GM-PhoRCC, ideal to study differences of X-ray properties of clusters.

To create a void catalogue in the Magneticum simulation data, we first applied a simple galaxy magnitude cut to obtain a sample of simulated galaxies approximately matching the mean number density of the BOSS LOWZ sample, and then used REVOLVER in the same way as for the galaxy data. It should be noted that the simple magnitude cut used means that the simulation galaxy sample does not exactly match the clustering properties of LOWZ galaxies, which also has an effect on the resultant void properties (Nadathur & Hotchkiss 2015). In particular, the bottom panel of Figure 1 shows that the Magneticum void sample is slightly shifted towards larger void sizes than LOWZ; however the difference is small and we will neglect it. In total, we obtained 40,000 voids in the simulation, which allows a statistically large sample to compare to the results from BOSS data.

When dealing with Magneticum voids, we bypass the time-consuming determination of the ellipsoidal axes for each void and instead approximate them as spheres. Knowing that this approximation is inaccurate, in Section 3 we introduce cuts designed to tackle this issue.

3 CLUSTERS IN DIFFERENT ENVIRONMENTS

3.1 Geometrical sample selection

Having a variety of cluster and void catalogues we can now begin to study the cluster properties as a function of their environment. In order to determine the environment in which the clusters reside, we use as a probe the location of the cluster within the large scale structure, i.e. whether a cluster is within a void or not.

We use the void catalogues described above to distinguish between clusters outside voids and those within voids. For each cluster and void pair, we determine the distance between the centres of the objects in units of the ellipsoidal axes (for BOSS voids) or the effective spherical radius (for Magneticum voids) and compare it with the distance from the void centre to the nearest boundary of the void. If the cluster-void distance is smaller than the boundary distance, then the cluster is assumed to be within the void.

However, for the case of complicated void geometries, even when the above condition is satisfied, the whole of the cluster may not truly lie within the void. In addition, clusters that are close to void boundaries are likely to be part of overdensities within filaments and walls at the void edge and not lie in true underdense regions. To be conservative, we therefore consider the following three cases:

(i) the clusters residing in the inner 70% of the ellipsoidal/spheroid void radius (IV7 category),
(ii) the clusters residing in the inner 50% of the ellipsoidal/spheroid void radius (IV5 category) and
(iii) the clusters outside voids (OV category).

We believe that the more conservative the threshold of the distance is the less contamination the sample has from clusters belonging to more overdense regions, hence the IV5 category should contain clusters that are well within the realistic 3-dimensional voids.

3.2 Density-based sample selection

In order to remove any concern about the effect of the irregular shapes of the voids on the clusters’ assigned environment based on the simple geometrical selection that we discussed above, we also estimate the local densities of the clusters’ environments directly, rather than using void location as a proxy.

We calculate the galaxy number density within a shell with 10 Mpc inner and 20 Mpc outer radius from the cluster centre using the physical coordinates of either SDSS DR13 photometric galaxy catalogue (Albareti et al. 2017) or the Magneticum galaxy catalogue. We choose this specific shell in order to safely exclude the galaxies that belong to the cluster in the local density calculation. When studying the observational catalogues, we introduce a cut on redshift where the SDSS photometry becomes incomplete, at $z = 0.5$. With this, we avoid including biases in the density estimation of clusters with $z > 0.5$ from areas where the galaxy population is sparser. We then split the clusters in ten density bins, each bin having equal number of clusters. For the comparisons of cluster properties we consider three cluster categories:

(i) the clusters in the lowest density bin, the clusters in the most underdense regions (LD category),
(ii) the clusters in the highest density bin, the clusters in the most overdense regions (HD1 category) and
(iii) the clusters in the second highest density bin, the clusters in overdense regions (HD2 category).

We include the HD2 category as an additional check, because the HD1 bin covers a very broad range of density values (see Figure 3), which may affect comparisons.

3.3 Comparing properties

Having assigned clusters to different environments we are ready to compare the distributions of their various properties. To do so, we use two different non-parametric statistical tests that compare continuous distributions without the need of an input comparison distribution, the Kolmogorov-Smirnov k-sample test (KS hereafter, Smirnov 1948) and the Anderson-Darling test (AD hereafter, Coronel-Brizio & Hernández-Montoya 2010). Both tests measure a “difference” between the distributions in question and their default distribution and report a p-value which shows the statistical significance of the result. AD test applies larger weights to the tails of the distributions and therefore is more sensitive in that area. The null hypothesis for both samples is that the samples compared are drawn from the same population.

For every cluster property in question, we compare the distribution of the clusters outside voids (OV category) with one of the two clusters in voids distributions (IV7 or IV5 category) as well as the clusters in underdense regions (LD category) with the clusters in overdense regions (HD1 and HD2 categories). Eventually we have four KS test results, one for each of the four comparisons, and four AD test results for the same comparisons. Non-zero KS or AD statistic value and p-value less than 0.05 means that the null hypothesis of the two tests that the distributions come from the same parental distribution can be rejected with 95% probability. We initially use both tests for our results, but after ensur-
ing they qualitatively provide the same results, we continue using only KS test which is more efficient computationally.

A KS or AD test p-value lower than 0.05 might not necessarily mean that the given property is different between two different cluster distributions; differences could arise randomly from a selection of clusters in the field population. For that reason, we create a verification test, which samples multiple times randomly the field population of clusters and ensures that the differences found using the KS and AD tests are not due to random selection.

3.4 Matched samples

We want to ensure that any differences between the properties of the cluster populations are not due to the difference of other properties that have already shown signs of differences. Therefore, we will always match the redshift and richness or mass distributions of the clusters in different environments, if available, before comparing their luminosity, temperature or other properties, in order to ensure that any difference found in the latter properties is not a product of differences in the redshift or richness/mass distributions.

For XCS DR2–SDSS we have three properties in hand, the redshift $z$, the bolometric X-ray luminosity $L_X$ and the temperature $T_X$. We first compare the redshift between the clusters within and out of voids and clusters in underdense and overdense regions. We use the nearest neighbours algorithm on the normalised cluster redshifts with a linking radius of 0.1 to match each cluster within voids (each cluster in underdense region) with a cluster outside voids (a cluster in underdense region). The linking radius or length represents the maximum distance between the normalised redshifts of two clusters that is used by the nearest neighbours algorithm to consider them matched. The pair of cluster samples in comparison have now the same size and are matched in $z$. We then compare the $L_X$ and $T_X$ of the matched samples. The same procedure is followed for the Magneticum clusters, with the only difference being that instead of initially matching the samples by their redshift, we match them by the cluster mass $M$. The cluster catalogue comes from the same snapshot in redshift, therefore all clusters have the same redshift.

For GMPhoRCC and redMaPPer the process is more complicated. After matching samples by redshift and achieving same sample size, we compare the richness of the $z$-matched samples. We then use the nearest neighbours algorithm and find for each cluster within voids (cluster in overdense region) the closest cluster outside voids (cluster in underdense region) in the two-dimensional space of redshift and richness. We use their normalised values and a linking length of 0.1. The new samples have the same size as the $z$-matched ones, but they are now matched by both $z$ and richness. Using those samples, we then compare the rest of the properties available for each of the cluster catalogues, such as the $L_X$ and $T_X$.

| Cluster catalogue | IV7 | IV5 | density bin |
|-------------------|-----|-----|-------------|
| XCS DR2–SDSS      | 24  | 14  | 69          |
| GMPhoRCC          | 67  | 37  | 105         |
| redMaPPer full    | 34,523 | 20,061 | 31,774 |
| redMaPPer 1       | 5,088 | 2,970  | 3,271      |
| redMaPPer 2       | 5,420 | 3,143  | 3,992      |
| redMaPPer 3       | 1,724 | 992    | 1,534      |
| redMaPPer X-ray   | 130  | 76    | 240        |
| Magneticum        | 28,125 | 17,672 | 35,312     |

4 RESULTS

4.1 Number of clusters

We search for clusters within and outside voids in both the observational and simulation catalogues and report the number of them on the third and fourth columns of Table 1. The number of clusters within and outside voids is the same for each catalogue because we match the cluster samples outside voids to the clusters within voids. We also calculate the density of the cluster environment and report the number of clusters in each of the equal-sized bins on the last column of Table 1. We can see that the X-ray selected observational catalogues, XCS DR2–SDSS and GMPhoRCC have a smaller number of clusters, while redMaPPer and Magneticum contain thousands of clusters in each category, ideal for providing statistical significance to our results.

For each of the cluster catalogues we count the number of clusters of each density bin that are found within and outside voids (Figure 3). One would expect that clusters with low background density would more likely be found within voids and that clusters with high background density would be more likely found outside clusters, i.e. that more clusters would be found within voids in the low background density bins and vice versa. Looking at Figure 3, in general, the background cluster density does not seem to relate to whether the cluster resides within a void or not. For the redMaPPer full catalogue, we find that the number of clusters found inside voids is larger at lower background densities, and smaller at high background density. For the other catalogues, the number of clusters in voids is approximately constant across all density bins, showing that splitting clusters within and outside large voids does not necessarily trace the density of their local environment.

The brown dashed horizontal lines on Figure 3 represent the number of clusters we would expect to find within voids considering the percentage of the survey volume contained within voids in each case. The fact that this number is much higher than the number of clusters in voids found is possibly due to the fact that clusters are assumed to be ellipsoids (for XCS DR2–SDSS, GMPhoRCC and redMaPPer full) or spheroids (for Magneticum) as opposed to their true 3-dimensional shapes. Voids with that approximated shape may overlap with each other and contain less clusters overall compared to the number they would contain if they had their real 3-dimensional shape. This reinforces the decision...
of having conservative cuts when studying clusters in voids; we have only used clusters within 50% or 70% the void radius.

We note here that summing the number of clusters within and outside voids in each density bin in the observational catalogues in Figure 3 does not result to the number of clusters in each density bin that is shown in Table 1. This is because the clusters within/outside voids have gone through a redshift cut in order to match the redshift range of the BOSS voids catalogue. Figure 3 also confirms the importance of our conservative cuts when studying clusters in voids; we have only used clusters within 50% or 70% the void radius.

4.2 Redshift distributions

As explained earlier, we begin with comparing the redshift distribution of clusters in the observational catalogues between the clusters within/outside voids and in overdense/underdense regions. For both XCS DR2–SDSS and GMPhoRCC, no differences are found when looking at cluster environment by geometrical criteria, but significant differences that are not associated with random selection were found when comparing clusters by their background density. The lack of differences seen in the former case might be a reflection of the low number statistics of clusters within and outside voids in both catalogues. On the other hand, redMaPPer clusters in different environments present significant differences in their redshift distributions, no matter how the environment is defined and in the full, all three subsamples and the X-ray subsample of the catalogue. In all cases where differences were found, it is seen that more clusters reside within low-density environments in low redshifts, a fact that could be explained by the expansion of the Universe and our use of physical coordinates to calculate the clusters’ local density.

The different redshift distributions between the cluster samples confirm the need to use matching samples in redshift from now on. Any difference found between other cluster property distributions will not be an effect of the different redshift distributions. The redshift distributions compared, along with the matched ones, are shown in Figure 4. The distributions on the left panels flatten at $z \sim 0.4$ because of the absence of voids at that redshift range - it is roughly the high-$z$ end of the LOWZ voids and the low-$z$ end of the CMASS voids.

4.3 Mass and richness distributions

For Magneticum clusters, we have a single redshift slice, hence the redshift of all clusters is the same, we perform matching on the cluster mass. We find that the definition of the environment here plays a role in the comparisons. The mass distributions of clusters with different background densities are significantly different from each other, while there is no difference found between the clusters within and outside Magneticum voids. This is a hint that the geometrical classification of the cluster environment might be naive, given the irregular shape of voids that is here modeled as spherical and the fact that Magneticum contains a larger amount of voids than the BOSS catalogues. Once again, after comparing the mass distributions, we match the catalogues to have as similar mass distributions as possible before we compare other properties. The distributions compared along with the matched ones are shown in Figure 5.

For GMPhoRCC and redMaPPer, where richness estimators of the clusters are available, $n_{200}$ and $\lambda$ respectively, we compare those between clusters in different environments with matched redshift distributions. For GMPhoRCC catalogues, significant differences between the richness estimator of the clusters are found between clusters in overdense and underdense regions (HD1-LD $p$-value < 0.001), but not between clusters within and outside voids (IV7-OV $p$-value = 0.41). For the redMaPPer catalogue, in both definitions of environment and in all four (sub)catalogues and the X-ray subsample, the richness distributions of clusters present significant differences, with KS $p$-values very close to zero (HD1-LD and IV7-OV $p$-value < 0.001). After comparing the richness distributions, we match the samples in both redshift and richness for the GMPhoRCC and redMaPPer catalogues, before moving on to compare the rest of the properties.

Those comparisons show clear signs that clusters inside voids and in underdense regions have lower number of galaxy members but similar redshift distribution to clusters outside voids and in overdense regions respectively.

It is worth noting here that the difference found between the richness distributions of clusters in different environments could be an artefact of the algorithm used to calculate the cluster richness. Concerning the redMaPPer catalogue, it has been shown that, during the richness estimation, projection effects depend on both the background galaxy density field and the large cluster-to-cluster fluctuations on the density field. The former only boosts the cluster richness by an unimportant amount and the latter can affect severely 5-15% of the clusters (Rozo et al. 2011). The richness estimation of a small percentage of redMaPPer clusters might be affected by the large scale structure density field and hence the presence of a cluster in a void or an overdensity. As for the XCS DR2–SDSS and GMPhoRCC catalogues, the richness bias inserted by GMPhoRCC during the richness calculation has also been estimated and it is smaller than the error of the richness calculation, therefore not significant (see calculation in Manolopoulou 2019).

We can see if the differences found between the different cluster populations can significantly affect cosmological studies that use galaxy clusters by measuring the cluster richness functions for the redMaPPer clusters and the mass functions for the Magneticum clusters. XCS DR2–SDSS and GMPhoRCC catalogues do not have large enough numbers of clusters for this purpose. The richness functions are good approximation of the cluster mass functions since richness has proven to be a good mass proxy for galaxy clusters for redMaPPer SDSS DR8 clusters (Baxter et al. 2016).

We construct the richness functions of the redMaPPer clusters and the mass functions of the Magneticum clusters and present them in Figure 6. The top panels show the richness and mass functions of redMaPPer (full) and Magneticum clusters respectively within and outside voids and the bottom ones show the same functions but for clusters in overdense and underdense regions. The middle panels are constructed as the top ones, but the clusters within voids functions are normalised with respect to the clusters out-
Figure 3. The number of clusters in and out of voids in each density bin for XCS DR2–SDSS (top left), GMPhoRCC (top right), redMaPPer full (bottom left) and Magneticum (bottom right) cluster catalogue. The brown dashed line shows the number of clusters we would expect in voids considering the percentage of the volume survey that are voids.

Figure 4. The normalised cumulative redshift distributions of XCS DR2–SDSS (left), GMPhoRCC (middle) and redMaPPer full (right) clusters in IV7 and OV categories (upper panels) and most overdense and most underdense regions (lower panels). Once redshift distributions are compared, the OV and LD categories are matched to the IV7 and HD1 ones respectively and the p-values of their comparisons are shown on the top of the graphs. The redMaPPer matched distributions match the IV7 and HD1 distributions very well and therefore are not distinguishable in the graph.
of the cluster environment, we find significant differences
between the X-ray luminosity of the clusters in overdense
and underdense regions and within and outside voids that
are confirmed by our random test (HD1-LD and IV7-OV
p-value < 0.001). For redMaPPer X-ray, we find significant
differences of the X-ray luminosity distributions between
the OV-IV7 samples (KS p-value = 0.007) and not between
the OV-IV5 samples (KS p-value = 0.104) - we also find signif-
cicent differences between the HD1-LD and HD2-LD samples
(KS p-value < 0.001 in both cases). The distributions of
X-ray luminosity of the HD1 and LD samples are shown
in Fig. 7. For XCS DR2–SDSS and Magneticum catalogues
we find significant differences between the X-ray luminos-
ity of the clusters in overdense and underdense regions only,
confirmed by our random test. For XCS DR2–SDSS, in the
HD1-LD case the KS p-value is smaller than 0.001 and in
OV-IV7 case the KS p-value is 0.62. For Magneticum, in the
HD1-LD case the KS p-value is smaller than 0.001 and in
OV-IV7 case the KS p-value is 0.55. Voids and underdense
regions host higher numbers of low luminosity clusters com-
pared to overdense regions and regions outside voids.

X-ray temperatures show more consistent between cat-
alogues. When splitting clusters within and outside voids,
in all cluster catalogues (XCS DR2–SDSS, GMPhoRCC,
redMaPPer X-ray and Magneticum) no significant differ-
ces are found in the X-ray temperature distributions of
clusters within/outside voids (OV-IV7 KS p-value ~ 0.21,
0.41, 0.05 and 0.62 respectively). When splitting clusters
according to the density of their environment, significant
differences are found in all catalogues in the X-ray tem-
perature distributions of clusters in overdense and under-
dense regions, confirmed by our random test (all HD1-LD
KS p-values < 0.001). In Fig. 7 we present the distribu-
tions of X-ray temperature of the HD1 and LD samples.
High-temperature clusters are more prevalent in overdense
regions and low-temperature clusters are more prevalent in
underdense regions.

4.5 Cluster galaxy populations

GMPhoRCC and redMaPPer catalogues contain some addi-
tional optical properties of the clusters and allow us to study
possible differences of those properties in clusters within dif-
ferent environments. GMPhoRCC optical properties contain
the CMR fitting properties and the colour of the red se-
quence of the clusters (Hood & Mann 2017, for more infor-
mation on these properties), while redMaPPer contains the
i-band cluster luminosity as well as the i-band magnitude
and luminosity of the BCG of the clusters.

The CMR intercept, gradient and width distributions of
clusters in overdense and underdense regions present signifi-
cant differences confirmed by the random test (HD1-LD KS
p-value ~ 1.5 \times 10^{-3}, < 0.001 and 6.7 \times 10^{-3} respectively);
the red sequence colour distributions are significantly differ-
ent between clusters in different environments no matter the
environment definition (HD1-LD and IV7-OV KS p-value
< 0.001). Those results suggest that clusters in overdense
regions tend to have flatter and narrower CMRs and redder
g–r colours, meaning that the environment is affecting the
properties of the galaxy populations in the clusters as well as
of the intracluster gas. When looking at the BCG properties
(i-band magnitude and luminosity) and the i-band cluster
luminosity, those are significantly brighter in the i-band in
clusters in overdense regions and outside voids compared to clusters in underdense regions and inside voids (all KS p-values are smaller than 0.001).

5 SAMPLE SIZE

The redMaPPer and Magneticum cluster catalogues offer a large number of clusters, large enough to enable the study of the dependence of the detected differences between two distributions of cluster properties to the number of clusters available. To this end, we take 100 random subsamples of various sizes from each of the two cluster catalogues and compare clusters within/outside voids and in overdense/underdense regions. We present the number of realisations we find significant differences between the cluster samples.

We choose to compare the luminosity distributions (i-band for redMaPPer full and X-ray for Magneticum) of clusters within 70% of the voids radius and outside voids and of clusters in the most overdense and most underdense regions. In Table 2 we show the number of times we find that the luminosity distributions are significantly different when we use random subsamples of the initial catalogues. The sample size seems to affect the two catalogues in different degree. For Magneticum, the difference in the X-ray luminosity distributions of clusters within and outside voids has already disappeared when we take 70% of the initial Magneticum cluster sample. In the case of comparing overdense and underdense regions, the difference signal is degrading slower and smoother; it is fully observed when taking 70% of the initial sample and degraded to half when taking 20% of the initial sample. In the redMaPPer full catalogue, the signal is a lot more persistent compared to the Magneticum catalogue signal and slowly degrades with the sample size when we compare the within voids and outside voids cluster distributions. The signal remains fully detected in all sample sizes when we compare clusters in overdense and underdense re-
Environmental dependence of X-ray and optical properties of galaxy clusters

Figure 7. The normalised cumulative X-ray luminosity (top) and temperature (bottom) distributions of redMaPPer X-ray clusters in most underdense (LD) and most underdense (HD1) cluster categories.

Table 2. The number of realisations (out of 100) where the luminosity distributions of redMaPPer and Magneticum clusters in different environments are found significantly different. For the Magneticum catalogue, we take subsamples of 70%, 50% and 20% of the initial catalogue, while for redMaPPer we take subsamples of 50%, 10% and 5% of the initial catalogue.

| Environment | 70% | 50% | 20% |
|-------------|-----|-----|-----|
| OV-IV7 comparison | 8 | 3 | 2 |
| LD-HD1 comparison | 100 | 95 | 52 |

| Environment | 50% | 10% | 5% |
|-------------|-----|-----|-----|
| redMaPPer full | 100 | 100 | 100 |

6 CONCLUSIONS

In this work, we studied the difference of the distributions of some main properties of galaxy clusters that reside in various environments, either defined by geometrical criteria or the local density. Our main findings include:

- The redshift distributions of clusters within environments of different densities present significant differences - there are more clusters within low-density environments in low redshifts compared to the high-density environments. No significant differences were found for clusters residing within and outside voids. Those results are consistent for XCS DR2–SDSS, GMPhoRCC and redMaPPer catalogues.
- The mass distribution of Magneticum clusters and the richness distribution of GMPhoRCC and redMaPPer clusters depend on the environment, with more massive and richer clusters being more prevalent in more overdense regions and outside of voids.
- X-ray luminosity and temperature distributions of clusters seem to differ within different environments across all the catalogues, with clusters with higher luminosity and temperature more likely to appear in overdense regions and outside of voids.
- Clusters in overdense regions tend to have flatter and narrower CMRs, with redder $g−r$ colours and more luminous BCGs when matched by redshift, as revealed from the GMPhoRCC and redMaPPer catalogues, so that the environment is affecting the properties of the galaxy populations in the clusters as well as of the intracluster gas.
- Local density-defined cluster samples often yield significant results when the geometrically-defined samples do not, suggesting that the former is more physically-motivated way to define samples than the latter.
- Possible implications on the cluster mass calibrations in various environments could occur as a result of the above, that would consequently affect cosmological parameters estimated based on those mass calculations.

In all cases, the sense of these differences is as expected from our initial intuition about clusters in underdense regions having had quieter merger histories, so that they could accrete less mass through mergers over their lifetime. The results concerning the mass and richness distributions are in agreement with the theoretical work presented in Cautun et al. (2014), where underdense regions were found to be devoid of massive galaxy clusters. Similar conclusions were shown in Aragón-Calvo et al. (2010), where the Cosmic Web was classified using morphological criteria instead of density criteria.

In Farahi et al. (2019), it is shown that clusters with lower X-ray luminosities and younger BCGs have also lower X-ray temperatures, which is in qualitative agreement with our results of difference between the X-ray luminosity and
temperature distributions of clusters within overdense and underdense regions. The signal of differences on the X-ray temperature distributions is not present when looking at clusters within and outside voids, while it is detectable for the case of X-ray luminosity distributions, possibly due to the difference in scatter between the two properties (as presented in Table 2 in Farahi et al. (2019)). The fact that the signal is not present for temperature distributions between clusters within and outside voids could be due to the difficulty of approximating general non-spherical void shapes as ellipses/spheres, as that might also increase the scatter of the properties.

Similar findings to ours were reported by other studies of differences in properties of galaxies in various environments (e.g. Hoyle et al. 2012). Just like their host clusters, galaxies in clusters in underdense regions seem to be younger, hence their bluer colour, and as a result spirals, as opposed to more old, elliptical galaxies found in clusters outside voids and in overdense regions. The cluster environment seems to affect the evolution of their galaxy members, not only their BCG. These effects could have important implications for precision cosmology with clusters of galaxies, since cluster mass calibrations can vary with environment.

Further research with larger observational X-ray cluster catalogues such as from the future eRosita mission (Predehl et al. 2010) will be invaluable to further study this effect with more accuracy and give more definitive results.

ACKNOWLEDGEMENTS

We thank the referee for the useful comments that helped to improve the publication. M.M. would like to thank D. Rapetti for the useful discussions and ideas on the cluster mass functions. M.S. was supported by the Olle Engkvist Foundation Project No. 2016/150, the Lundström–Rapetti for the useful discussions and ideas on the clusters, and a P. E. Flién fellowship (Uppsala University). S.N. was supported by UK Space Agency grant ST/N00180X/1.

DATA AVAILABILITY

The data underlying this article will be shared on reasonable request to the corresponding author.

REFERENCES

Albamonte M., van de Weygaert R., Jones B. J. T., 2008, in Plionis M., López-Cruz O., Hughes D., eds, Lecture Notes in Physics, Berlin Springer Verlag Vol. 740, A Pan-Chromatic View of Clusters of Galaxies and the Large-Scale Structure, p. 24 (arXiv:astro-ph/0605575), doi:10.1007/978-1-4020-6941-3_9

Cautun M., van de Weygaert R., Jones B. J. T., Frenk C. S., 2014, MNRAS, 441, 2923

Coronel-Brizio H. F., Hernández-Montoya A. R., 2010, Physica A Statistical Mechanics and its Applications, 389, 3508

Darvish B., Scoville N. Z., Martin C., Mobasher B., Diaz-Santos T., Shen L., 2018, ApJ, 860, 111

Davies M., Efstathiou G., Frenk C. S., White S. D. M., 1985, ApJ, 292, 371

Dawson K. S., et al., 2013, AJ, 145, 10

Dolag K., Borgani S., Murante G., Springel V., 2009, MNRAS, 399, 497

Dressler A., 1980, ApJ, 236, 351

Farahi A., et al., 2019, Nature Communications, 10, 2504

Finoguenov A., et al., 2020, A&A, 638, A114

Giles P., Manolopoulou M., et al. 2020a, to be submitted to MNRAS

Giles P., Bermeo A., et al., 2020b, to be submitted to MNRAS

Gupta N., Saro A., Mohr J. J., Dolag K., Liu J., 2017, MNRAS, 469, 3069

Hilton M., et al., 2018, ApJS, 235, 20

Hirschmann M., Dolag K., Saro A., Bachmann L., Borgani S., Burkert A., 2014, MNRAS, 442, 2304

Hood R. J., Mann R. G., 2017, MNRAS, 469, 3851

Hoyle F., Vogeley M. S., Pan D., 2012, MNRAS, 426, 3041

Komatsu E., et al., 2011, ApJS, 192, 18

Kovács A., 2018, MNRAS, 475, 1777

Kravtsov A. V., Borgani S., 2012, ARA&A, 50, 353

Liao S., Gao L., 2019, MNRAS, 485, 464

Lloyd-Davies E. J., et al., 2011, MNRAS, 418, 14

Manolopoulou M., 2019, The University of Edinburgh, https://era.ed.ac.uk/handle/1842/35894?show=full

Matthews D. J., Newman J. A., Coil A. L., Cooper M. C., Gwyn S. D. J., 2013, ApJS, 204, 21

Mehrtens N., et al., 2012, MNRAS, 423, 1024

Meneux B., et al., 2006, A&A, 452, 387

Migkas K., Schellenberger G., Reiprich T. H., Poczyň F., Ramos-Ceja M. E., Lovisari L., 2020, A&A, 636, A15

Nadathur S., 2016, MNRAS, 461, 358

Nadathur S., Crittenden R., 2016, ApJ, 830, L19

Nadathur S., Hotchkiss S., 2014, MNRAS, 440, 1248

Nadathur S., Hotchkiss S., 2015, MNRAS, 454, 889

Nadathur S., Carter P. M., Percival W. J., Winther H. A., Bautista J. E., 2019, Phys. Rev. D, 100, 023504

Neyrinck M. C., 2008, MNRAS, 386, 2101

Poulad A., Heinämäki P., Nurmi P., Teerikorpi P., Tempel E., Poutanen J., 2010, Phys. Rev. D, 100, 023504

Predehl P., et al., 2010, X-ray Astronomy 2009: Present Status, Multi-Wavelength Approach and Future Perspectives, 1248, 543

Raghunathan S., Nadathur S., Sherwin B. D., Whitehorn N., 2019, arXiv e-prints, p. arXiv:1911.08475

Reid B., et al., 2016, MNRAS, 455, 1553

Ricciardelli E., Cava A., Varela J., Tamone A., 2017, ApJ, 846, L4

Roxo E., Rykoff E., Koester B., Nord B., Wu H.-Y., Evrard A., Wechsler R., 2011, ApJ, 740, 53

Rykoff E. S., et al., 2014, ApJ, 785, 104

Sahlén M., et al., 2009, MNRAS, 397, 577

Scodellino M., et al., 2018, A&A, 609, A84

Smirnov N., 1948, Ann. Math. Statist., 19, 279

Spiegel E. A., 1999, in Harvey A., ed., On Einstein’s Path: essays in honor of Engelbert Schucking, p. 465 (arXiv:astro-ph/9801014)

Springel V., White S. D. M., Tormen G., Kauffmann G., 2001, MNRAS, 328, 726

Springel V., Frenk C. S., White S. D. M., 2006, Nature, 440, 1137

Varela J., Betancort-Rijo J., Trujillo I., Ricciardelli E., 2012, ApJ, 744, 82

Wang L., et al., 2018, A&A, 618, A1

MNRAS 000, 1–13 (2020)
