Remote Synchronization Simulation of Onboard Crystal Oscillator for QZSS Using L1/L2/L5 Signals for Error Adjustment

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A new error adjustment method for remote synchronization of the onboard crystal oscillator for the quasi-zenith satellite system (QZSS) using three different frequency positioning signals (L1/L2/L5) is proposed. The error adjustment method that uses L1/L2 positioning signals was demonstrated in the past. In both methods, the frequency-dependent part and the frequency-independent part were considered separately, and the total time information delay was estimated. By adopting L1/L2/L5, synchronization was improved by approximately 15% compared with that using L1/L2 and approximately 10% compared with that using L1/L5 and a synchronization error of less than 0.77 nanosecond was realized.

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1. INTRODUCTION

The Japanese Quasi-Zenith Satellite (QZS) System (QZSS) is a three-satellite navigation/positioning system conceived to improve the positioning performance (satellite availability and position accuracy) of the presently available global positioning system (GPS) in urban areas where high-rise buildings reduce the number of visible GPS satellites [1]. A new timekeeping method of the QZSS, named the remote synchronization system for an onboard crystal oscillator (RESSOX), has been planned by the National Institute of Advanced Industrial Science and Technology (AIST, Tsukuba, Japan) [2]. RESSOX is a remote-control method that permits synchronization between a ground station standard and QZS clocks. In its original concept, various delay models are used for the estimation of the delay of the RESSOX control signal that includes time information of QZSS time and is advanced with respect to QZSS-time to compensate the delay during transmission. This is considered to be the feed-forward control. Furthermore, pseudoranges of positioning signals obtained at the ground station, named the time management station (TMS), are used for error adjustment, where QZSS-Time is a standard time of QZSS, like GPS time for GPS, and refers to UTC (NICT). This is considered to be the feedback control. RESSOX is realized by combining feed-forward and feedback control. The RESSOX control signal is transmitted with the Ku-band from the TMS.

The proposed Japanese QZSS has the following properties regarding its timekeeping system (TKS): (1) it is possible to control the system over a 24-hour period as long as good visibility of QZS is obtained; (2) a high-stability crystal oscillator is superior to an atomic standard in terms of short-term frequency stability [3]; and (3) the QZSS employs a maximum of three satellites, which are not too many to monitor from the ground.

RESSOX reduces overall costs, satellite power consumption, and onboard weight and volume; and it has a longer lifetime than a system with onboard atomic clocks.

RESSOX ground experiments and computer simulations have been conducted since 2003. QZS broadcasts four
positioning signals as availability enhancement signals: L1C/A, L1C, L2C, and L5 [4]. The tentative target of our research is synchronization to within 10 nanoseconds between the ground standard time and the QZS site at any time and frequency stability better than $1 \times 10^{-13}$ for 100,000 seconds. Initial experimental results using only L1/L2 positioning signals and experimental apparatus have been introduced previously [5–10]. We have developed a new feedback method that uses L1/L2/L5 positioning signals of the QZS and proved that we could improve synchronization by 15% compared with the former L1/L2 method. Since experimental apparatus for L5 are not available at the moment, only simulation results are presented in this paper.

Evaluations of the effects of the range error magnitude and the least-squares filter used at the ground site are also discussed.

2. SIMULATION MODEL

To investigate this new RESSOX method, a specific software simulator has been developed. The actual onboard crystal oscillator is MINI-OCXO manufactured by C-MAC MicroTechnology (Buckinghamshire, UK), and is modeled as follows:

$$f = 1.023 \times 10^7 \left(1.0 + 3.2500048 \times 10^{-8} (V - 5.352333)\right),$$  \hspace{1cm} (1)

where $f$ is the output frequency and $V$ is the applied voltage (when $V = 5.352333$ V, $f = 10.23$ MHz).

To control MINI-OCXO using the difference between uplinked time information with RESSOX control signal and MINI-OCXO time, modified PI control of the control voltage was employed. The following formula that describes modified PI control was used:

$$v_k = \text{offset} - \frac{k_1}{l + 1} \sum_{i=k-l}^{k} (t_{\text{OCXO}} - t_{\text{RESSOX}})_i$$
$$- k_2 \sum_{i=0}^{k} \int_{i}^{\infty} (t_{\text{OCXO}} - t_{\text{RESSOX}}) \, dt.$$  \hspace{1cm} (2)

Here, $v_k$ is the $k$th output voltage, offset = 5.352333 V, $k_1$ is a proportional gain set at $7.0 \times 10^6$, $k_2$ is an integral gain set at $3.0 \times 10^4$, $l$ is the number of past data used for proportional control and is set at 1, $k$ is the data number from the beginning of the simulation, $p$ is the integral interval, which means an overlapping integral number, set at 2, and $t_{\text{RESSOX}}$ is time information of the received RESSOX control signal.

Control repetition at the TMS is once every second, and that on the QZS is once every 1.5 seconds.

The simulation conditions are shown in Table 1. Typical Keplerian orbit elements of the QZS, shown in Table 1, were assumed. To calculate the orbit precisely, the EGM96 geopotential model with the spherical harmonic coefficient of degree and order 360, the gravity effects of the sun, the moon, and other planets taken from the Jet Propulsion Laboratory (JPL, NASA, Pasadena, Calif, USA) ephemeris DE405, the radiation pressure, and the solid tide effects were considered. To calculate ionospheric delay, data (COD10426.ION) from the Center for Orbit Determination in Europe (CODE, University of Bern, Bern, Switzerland) was used. The simulation period was all day, January 1, 2000. This means that positions of the sun, the moon, and other planets and ionospheric data for that day were used. The meteorological conditions for tropospheric delay calculation were assumed to be constant at $15^\circ$C, 1013.25 hPa, and 70% relative humidity, and the Saastamoinen model was used. The position of the TMS was assumed to be in Okinawa (26.5 N, 127.9 E, elevation = 0.0 m).

The calculations using these parameters correspond to the authentic range in Figure 1, and the “Orbit/Delay calculation (without error)” in Figure 2. These conditions can be expressed as $x = -22,881,059.583$ m, $y = -32,625,645.367$ m, $z = 19,898,922.824$ m, $v_x = 2,207.153$ m/s, $v_y = 839.448$ m/s, and $v_z = 1,693.581$ m/s as the initial conditions in the International Celestial Reference Frame (ICRF).

For the orbit information used at the TMS, an initial error of $-5$ m for each axis of ICRF, that is, the initial conditions of $x = -22,881,064.583$ m, $y = -32,625,640.367$ m, and $z = 19,898,917.824$ m of the equation of motion ($v_x$, $v_y$, and $v_z$ are the same as the authentic values) are assumed in order to create the time adjustment file for the transmitting time adjuster (TTA) and the database of L1/L2/L5 in Figure 2. The ionospheric and tropospheric delays were not considered. The differences in initial conditions between authentic delay and estimated delay are shown in Figure 1.

3. CONTROL METHOD

To realize RESSOX, L1, L2, and L5 pseudoranges were considered separately, and the delay of the frequency-dependent part (i.e., ionospheric delay) and that of the frequency-independent part (i.e., clock error, range error, and tropospheric delay) were estimated. The following is the simulation sequence of this new method, as shown in Figure 2. In the simulation, some experimental apparatuses, such as the onboard crystal oscillator (MINI-OCXO), TTA, the time comparator, and the QZS signal receiver are modeled based on the ground experiments.
 Initialization (Steps 1 to 3)

Step 1. Four estimated delays (L1-, L2-, L5-, and Ku-bands) are prepared. These estimated delays include model errors such as those due to the orbit, ionosphere, or troposphere, and we assume that they are used at the TMS as the measurement results. The estimated delays of the L1-, L2-, and L5-bands make up the database of L1, L2, and L5 delays in the RESSOX controller to be used for comparison with the L1-, L2-, and L5-band pseudoranges in Step 7. In contrast, the estimated delay of the Ku-band is described in the time adjustment file for TTA, and is used as feed-forward control.

Step 2. Four authentic delays (L1-, L2-, L5-, and Ku-bands) are prepared. These delays do not contain any errors. Three of these delays are contained in the L1, L2, and L5 authentic delay file, and the fourth one is contained in the Ku authentic delay file.

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**Table 1: Simulation conditions.**

| Items                        | Values                                      |
|------------------------------|---------------------------------------------|
| Simulation period           | 2000.1.1 00:00:00UTC-2000.1.2 00:00:00UTC  |
| Satellite cross section, m² | 30.0                                         |
| CODE data of ionosphere COD10426.ION |                                    |
| Semimajor axis, m           | 42164170.0                                   |
| Eccentricity, m             | 0.099                                        |
| Inclination, deg            | 45.0                                         |
| Right ascension of the ascending node, deg | 205.0                                      |
| Argument of perigee, deg    | 270.0                                        |
| Mean motion, deg            | 120.0                                        |
| Position of ground station  | 26.5 N, 127.9 E, Height = 0.0 m (Okinawa)    |
| Solid Earth tide            | Moon and Sun are considered, k2 = 0.3 (IAG 1999) |
| Geopotential model          | EGM96, n, m = 360                            |
| Other celestial bodies      | Moon, Sun, Mercury, Venus, Mars, Jupiter, Saturn, Uranus, Neptune, Pluto(JPL-DE405) |
| Satellite mass, kg          | 3000.0                                       |

**Figure 2: Simulation block diagram.** Number in parenthesis indicates the step explained in the text. Our goal is synchronization between a ground atomic clock at TMS and an onboard crystal oscillator on QZS.
Step 3. The time adjustment file for TTA is fed into the TTA as feed-forward control. The timing for transmitting time information using the RESSOX control signal is adjusted to give the time comparator the correct time when the signal arrives at the QZS.

Process routine (Steps 4–10)

Step 4. The delay of the RESSOX control signal during transmission is realized by the Ku authentic delay file.

Step 5. The onboard crystal oscillator is controlled using the time difference between the RESSOX control signal and the time of the crystal oscillator itself. Some noise generated by the crystal oscillator and the time comparator is assumed in this step and is generated by Stable 32, a clock-simulation software [11]. We assume that the onboard crystal oscillator has a stability of $1.0 \times 10^{-12}$ from 1 to 100 seconds and $5.0 \times 10^{-11}$ for one day (86400 s), giving random walk frequency noise $= 5.0 \times 10^{-14}$, flicker frequency noise $= 6.5 \times 10^{-13}$, and frequency drift per second $= 6 \times 10^{-16}$, and the time comparator has a stability of $2.5 \times 10^{-10}$ for 1 second and has only phase-white noise. The Allan deviation is shown in Figure 3.

Step 6. The pseudoranges of L1, L2, and L5 are calculated using the L1, L2, and L5 authentic delay file and the onboard crystal oscillator error. Noise that has 1 nanosecond standard deviation is added during transmission.

Step 7. The pseudoranges of L1, L2, and L5, obtained by the QZS signal receiver, are compared with the database of L1, L2, and L5 delay, and the differences between the pseudoranges and the database are designated as $E_1$ for L1 (frequency $f_{L1} = 1.57542 \times 10^9$ Hz), $E_2$ for L2 ($f_{L2} = 1.2276 \times 10^9$ Hz), and $E_3$ for L5 ($f_{L5} = 1.17645 \times 10^9$ Hz).

Step 8. Simultaneous equations (3), which include $E_1$, $E_2$, and $E_3$, delays due to the nonfrequency-dependent term $e$, and the coefficient of delay $k$ due to the frequency-dependent term (i.e., ionospheric delay) as unknowns, are solved:

$$e + \frac{k}{f_{L1}} = E_1, \quad f_{L1} = 1.57542 \times 10^9 \text{[Hz]},$$

$$e + \frac{k}{f_{L2}} = E_2, \quad f_{L2} = 1.2276 \times 10^9 \text{[Hz]},$$

$$e + \frac{k}{f_{L5}} = E_3, \quad f_{L5} = 1.17645 \times 10^9 \text{[Hz]}.$$  \hspace{1cm} (3)

These equations are expressed using a matrix as follows:

$$\begin{bmatrix} 1 & 1/f_{L1} & e \\ 1 & 1/f_{L2} & k \\ 1 & 1/f_{L5} & \end{bmatrix} \begin{bmatrix} E_1 \\ E_2 \\ E_3 \end{bmatrix} = \begin{bmatrix} A \end{bmatrix} \text{ where } \begin{bmatrix} A \end{bmatrix} = \text{E.} \hspace{1cm} (4)$$

Since $A$ is not a square matrix, to solve the equations, pseudoinverse $x = (A^T A)^{-1} A^T E$ is used.

Step 9. Using the solutions of the simultaneous equations, we obtain the time to be adjusted with formula (5), of the RESSOX control signal using the Ku-band ($f_{Ku} = 1.43453 \times 10^{10}$ Hz) for the TTA

$$e + k/f_{Ku}, \quad f_{Ku} = 1.43453 \times 10^{10} \text{[Hz]}. \hspace{1cm} (5)$$

Step 10. As a result of combining the delay estimation file in Step 3 and the time to be adjusted for the TTA, the TTA is controlled. This process is considered to be the feedback control. We consider some filters in this step, as described later. Then we go back to Step 4. The calculation of the time to be adjusted is conducted every second. The default filter is constructed using 100 data values of the time to be adjusted (result of formula (5) using the difference between measured pseudoranges of L1/L2/L5 and estimated pseudoranges of L1/L2/L5 prepared as the database of L1/L2/L5 delay) from 6 to 105 seconds before every second. In our first consideration, the change of the time to be adjusted would depend on mainly the tropospheric delay in Figure 4. Since tropospheric delay depends on the elevation angle, the change of tropospheric delay can be approximated in the first order for such
a short period as 100 seconds. Therefore, 100 data values of
time to be adjusted are used for the first-order least-squares
filtering, and the time to be adjusted is extrapolated to the
current time, as shown in Figure 4. To calculate and send the
filtering result to the TTA as the time adjustment command,
six seconds are assumed to be required.

Control is conducted every second on the ground and ev-
every 1.5 seconds on the QZS. These control frequencies will be
actually adopted in the QZSS project.

In Figure 2, the three pink blocks indicate the key pro-
cesses of this method.

4. SIMULATION RESULTS

The simulation was conducted according to the block dia-
gram shown in Figure 2.

The atomic standard at the TMS and the onboard crys-
tal oscillator can be synchronized to within 1 nanosecond
throughout 24 hours, even though the noise of the pseu-
dorange has a 1 nanosecond standard deviation, as shown
in Figure 5. The change of range error during simulation
is shown in Figure 6. For the orbit information used at the
TMS, which corresponds to “Orbit/Delay calculation (with
error)” in Figure 2, an initial error of
\( T_{\text{MS}} \), which corresponds to “Orbit/Delay calculation (with
current time, as shown inFigure 4. To calculate and send the
filtering result to the TTA as the time adjustment command,
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is shown in Figure 6. For the orbit information used at the
TMS, which corresponds to “Orbit/Delay calculation (with
error)” in Figure 2, an initial error of \(-5\) m for each axis of
ICRF is assumed as measurement error. The difference in
range between authentic and measured errors corresponds
to the range error. Even though the range error (i.e., or-
bit estimation) is considerably large (0–12 m), the proposed
method functions correctly.

Using the solutions of \( e \) and \( k \) of simultaneous equa-
tions (3), the time to be adjusted was calculated. The two
terms of the time to be adjusted, that is, \( e \) and \( k/f_{Ku}^2 \), cor-
respond to delays other than ionospheric delay and to the
ionospheric delay of the RESSOX control signal using the
\( Ku \)-band. As shown in Figure 7, although \( e \) and \( k/f_{Ku}^2 \) of the
time to be adjusted vary by about ±30 nanoseconds and 0.5
nanosecond, respectively, because of the noise of the pseu-
dorange, the results of these solutions show good agreement
with the actual delays of these origins, that is, the range error
plus tropospheric delay and the ionospheric delay shown in
Figure 8.

The actual time adjustment command calculated using
a combination of 100 elements of the time to be adjusted
and the first-order least-squares filter shown in Figure 4 is
shown in Figure 9. Since the element of the time to be ad-
justed, \( k/f_{Ku}^2 \), is approximately two orders smaller than that
of the time to be adjusted, \( e \), the graph shape is similar to
that for \( e \) in Figure 7. The filter has the effect of reducing the
noise.

5. EFFECT OF ADOPTING THREE FREQUENCIES

To compare the effects of using three frequencies, synchro-
nization error was evaluated. Three different combinations
were investigated: L1 and L2, L1 and L5, and L1, L2, and
L5. The combination of L1 and L2 means the current usable
combination, and that of L1 and L5 means the most separate
frequencies for which a small error is expected. First, we con-
sidered the optimum number of data values with the first-
order least-squares filter. The number of data values was in-
creased to 1,000. The tendency of the number of data values
being greater with smaller synchronization error was con-
irmed, and the best results were obtained in the case of using
three frequencies, as shown in Figure 10. In any case, when
the number of data values was smaller than 50, the maxi-
mum synchronization error was larger than 10 nanoseconds,
and the smallest synchronization error was obtained when
the number of data values was 1,000. Synchronization us-
ing L1/L2/L5 was improved by approximately 15% compared
with that using L1/L2 and by approximately 10% compared
with that using L1/L5.

Next, we compared the effect of the order of the filter, us-
ing three frequencies; the results are shown in Figure 11. In
the case of the zeroth-order filter, when the number of data
values was small, the maximum synchronization error was
smaller than 3 nanoseconds; however, it increased when the
number of data values was larger than 200. In the case of a
first- or higher-order filter, when the number of data values
Figure 7: Elements of time to be adjusted. $e$ and $K/f_{K_a}^2$ correspond to the range error plus tropospheric delay and the ionospheric delay shown in Figure 8, respectively.

Figure 8: Authentic delay of range error plus tropospheric delay and ionospheric delay.

Figure 9: Actual time adjustment command calculated using a combination of 100 elements of time to be adjusted and first-order least-squares filter shown in Figure 4.

was small, the maximum synchronization error became unacceptably large. The smallest maximum synchronization error was obtained when the first-order filter and 1,000 samples were used.

6. CONCLUSIONS

This study is summarized as follows.

(1) A new error-adjustment method for remote synchronization of the onboard crystal oscillator (RESSOX) for the QZSS using L1/L2/L5 positioning signals was demonstrated by simulation.

(2) Synchronization to within 1 nanosecond between the onboard crystal oscillator and the ground standard time was achieved in a 24-hour simulation.

(3) The ionospheric delay and the combination of tropospheric delay and range error of the RESSOX control signal were estimated in the calculation and efficiently compensated.

(4) On the ground, the number of data values and the order of the least-squares filter can be changed. The first-order least-squares filter using 1000 data values and three frequencies is the best, yielding a synchronization error of less than 0.77 nanosecond.

(5) Synchronization using L1/L2/L5 was improved by approximately 15% compared with that using L1/L2 and by approximately 10% compared with that using L1/L5.
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