A comparative study of hyperspectral unmixing using different algorithm approaches

Ain Zat Mohd Yusof, Redzuan Abdul Manap, Abd Majid Darsono
Centre of Telecommunication Research and Innovation (CeTRI), Faculty of Electronics and Computer Engineering, Universiti Teknikal Malaysia Melaka (UTeM), Malaysia.

ABSTRACT
Hyperspectral unmixing (HU) is an important technique for remotely sensed hyperspectral data exploitation. Hyperspectral unmixing is required to get an accurate estimation due to low spatial resolution of hyperspectral cameras, microscopic material mixing, and multiple scattering that cause spectra measured by hyperspectral cameras are mixtures of spectra of materials in a scene. It is a process of estimating constituent endmembers and their fractional abundances present at each pixel in hyperspectral image. Researchers have devised and investigated many models searching for robust, stable, tractable and accurate unmixing algorithm. Such algorithm are highly desirable to avoid propagation of errors within the process. This paper presents the comparison of hyperspectral unmixing method by using different kind of algorithms. These algorithms are named VCA, NFINDR, SISAL, and CoNMF. The performance of unmixing process is evaluated by calculating the SAD (spectral angle distance) for each endmembers by using same input of hyperspectral data for different algorithm.

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Corresponding Author:
Redzuan Abdul Manap,
Centre of Telecommunication Research and Innovation (CeTRI), Faculty of Electronics and Computer Engineering, Universiti Teknikal Malaysia Melaka (UTeM), Hang Tuah Jaya, Durian Tunggal 76100 Melaka, Malaysia.
Email: redzuan@utem.edu.my

1. INTRODUCTION
The imaging concept is divided into two types which are multispectral and hyperspectral. It collects and processes the information from across the electromagnetic spectrum [1]. This concept enables capture of an image simultaneously in hundreds of narrow continuous spectral band. The advantage is it provides a large amount of data including of the complete spectrum of ground object due to problem of resolution limitation of the sensors and the variability of the ground surface. The observation of one pixel may contain several disparate substances causing it to be a “mixed pixel”. Furthermore, to utilize the hyperspectral information, these mixed pixel must be decomposed into a set of constituent spectra called endmember signatures and their corresponding proportions called abundances [1, 2]. Keeping in mind the end goal to make full utilization of the information, hyperspectral unmixing (HU) has becomes an essential produces, which deteriorates a mixed pixel into a gathering on constituent materials additionally called endmember and their relative proportions. HU alludes to any procedure that isolates the pixel spectra from a hyperspectral picture into a collection of constituent spectra, or spectral signatures, called endmembers and a set of fractional abundances, one set for each pixel [3]. The endmembers are for the most part expected to represent the pure materials present in the images and the set of abundances, or simply abundances at every pixel to represent to the level of each endmember that is available in the pixel. Over the last years, different HU algorithms are developed for each of the three main steps of the spectral unmixing chain [4]:
1) estimation of the number of endmembers in a scene; 2) identification of the spectral signatures of the endmembers; and 3) estimation of the fractional abundance of each endmember in each pixel of the scene. However, few algorithms can perform all the stages involved in the hyperspectral unmixing process. Such algorithms are highly desirable to avoid the propagation of errors within the chain [4]. For example, a signal unmixing methodology to extract pure vegetation signal from individual mixed pixel of scene consisting of soil and vegetation is proposed in [5]. In this paper, we study several hyperspectral unmixing (HU) algorithms, namely NFINDR [6, 7], VCA [8, 9], SISAL [10, 11], and CoNMF [12, 13]. The performance of their unmixing process is evaluated by calculating the spectral angle distance (SAD) for each endmembers using the same input of hyperspectral data [14, 15]. However, there is still no in-depth comparative study have been conducted for these well-known methods in hyperspectral unmixing process. So, the research will determine the performance of current unmixing method that can help with reliable detection and identification. It will give benefit to country especially in agriculture production that has been highly dependant on natural resources for centuries [16]. Other than that, it will also benefit on air pollution detection that give negative impact to health [17].

Figure 1 demonstrate the unmixing process that involving four main steps that are atmospheric correction, dimensionality reduction, unmixing, and inversion [18]. The first step is considering the atmospheric correction of the radiance data cube. The second step is data reduction after converting the property of data cube. The third step is unmixing, and the last step is inversion. Unmixing which may be tackled via the classical endmember determination plus inversion or via sparse regression or sparse coding approaches.

2. RESEARCH METHOD

Systematic models for the mixing of various materials provide the foundation for developing techniques to recover estimates of the constituent substance spectra and their proportions from mixed pixels. An entire model of the mixing procedure, in any case, is more muddled than a basic depiction of how surface mixing connect. Mixing models can likewise consolidate the impacts of the three-dimensional topology of items in a scene, for example, the tallness of trees, the size and thickness of their overhangs, and the sensor perception edge. The essential introduce of blend displaying is that inside a given scene, the surface is overwhelmed by few particular materials that have moderately consistent spectral properties. These particular substances (e.g., water, grass, mineral composes) are called endmembers, and the portions in which they show up in a blended pixel are called fragmentary plenitudes. On the off chance that the vast majority of the spectral fluctuation inside a scene is a result of endmembers showing up in differing extents, it legitimately takes after that some mix of their unearthly properties can demonstrate the otherworldly inconstancy saw by the remote detecting framework [19].
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Figure 2 illustrates how linear mixing radiation reflects from the surface. The way of the reflection in linear surface is portrayed as a checkerboard mixture and any given package of incident radiation only interact with one component for example no multiple scattering between components [20]. If the total surface area is considered to be divided proportionally according to the fractional abundances of the endmembers, then the reflected radiation will convey the characteristics of the associated media with the same proportions. In this sense, there exists a linear relationship between the fractional abundance of the substances comprising the area being imaged and the spectra in the reflected radiation [21].

2.1. Algorithms for hyperspectral unmixing
The resolution cell corresponding to a single pixel in an image contains several substances. In this situation, the scattered energy is a mixing of the endmember spectra [19, 22]. A challenging task underlying many hyperspectral imagery applications is then decomposing a mixed pixel into a collection of reflection spectra called endmember signatures. It also true that it is not exempt or drawbacks, such as the fact that all the possible combinations of algorithms in order to fully unmixing a hyperspectral image according to the aforementioned processing chain demand a formidable computational effort, which tend to be higher the better the performance of the designed unmixing chain is. The algorithms exploit two facts: 1) the endmember are the vertices of a simplex and 2) the affine transformation of a simplex is also a simplex [23].

2.2. N-FINDR algorithms
One of the earliest approaches is the N-FINDR algorithms is a selection algorithms. Its work is described as follow: it starts with a random collection of image pixel spectra, corresponding to the initial set of endmembers [24]. Then, each of the remaining image pixels is considered as a candidate to replace each endmembers, if doing so the volume of the simplex increases, then it is accepted. The N-FINDR algorithms require a dimension reduction step, originally an orthogonal subspace projection (OSP) to a space of dimension N-1, where N is the number of endmember [25, 26]. This set of endmembers found by the N-FINDR would not allow the nonnegative unmixing of the pixel spectra in general [7].

```matlab
if run_nfindr
    angles=Mtrue./(repmat(sqrt(sum(Mtrue.^2)),p,1)).*(repmat(sqrt(sum(Mnf.^2)),p,1)));
    P = zeros(p);
    for i = 1:p
        [dummy,j] = max(angles(i,:));
        P(j,i) = 1;
        angles(:,j) = inf;
    end
    FINDR_ERR=norm(Mtrue(:,1)-Mnf(:,1),'fro')/norm(Mtrue(:,1),'fro');
    angles=sum(Mtrue(:,1).*Mnf(:,1))./sqrt(sum(Mtrue(:,1).^2).*sum(Mnf(:,1).^2));
    FINDR_MAX_ANG = acos(min(angles(:)))*180/pi;
end
```

2.3. VCA algorithms
The vertex component analysis algorithms (VCA) are presented in this hyperspectral [8, 9]. This algorithm is unsupervised and exploits that the affine transformation of a simplex is also simplex. It works with projected and unprojected data [26, 27]. The algorithms iteratively projects data onto a direction orthogonal to the subspace spanned by the endmembers already determined. The new endmembers signature corresponds to the extreme of the projection. The algorithms iterates until all endmembers are exhausted.
VCA_ERR = inf;
VCA_MAX_ANG = inf;
if run_vca
angles=Mtrue./{repmat(sqrt(sum(Mtrue.^2)),p,1).}.*{repmat(sqrt(sum(Mvca.^2)),p,1)};
P = zeros(p);
for i = 1:p
[dummy,j] = max(angles(i,:));
P(j,i) = 1;
angles(:,j) = inf;
end
VCA_ERR = norm(Mtrue(:,1)-Mvca(:,1),'fro')/norm(Mtrue(:,1),'fro');
angles = sum(Mtrue(:,1).*Mvca(:,1))./sqrt(sum(Mtrue(:,1).^2).*sum(Mvca(:,1).^2));
VCA_MAX_ANG = acos(min(angles(:)))*180/pi;
end

2.4. SISAL algorithm

The SISAL (simple identification via variable splitting and augmented Lagrangian) algorithm also performs the endmember extraction for hyperspectral unmixing. The features of these algorithms are implementing a robust version of the minimum volume concept [10, 11]. It robustness allowing the positivity constrains to be violated in order to estimate endmember more precise. The noise vector is considered. The existing of noise or any other source, the spectral vectors may lie outside the true data simplex [28].

SISAL_ERR = inf;
SISAL_MAX_ANG = inf;
if run_sisal
angles=Mtrue./{repmat(sqrt(sum(Mtrue.^2)),p,1).}.*{repmat(sqrt(sum(Msisal.^2)),p,1)};
P = zeros(p);
for i = 1:p
[dummy,j] = max(angles(i,:));
P(j,i) = 1;
angles(:,j) = inf;
end
SISAL_ERR = norm(Mtrue(:,1)-Msisal(:,1),'fro')/norm(Mtrue(:,1),'fro');
angles = sum(Mtrue(:,1).*Msisal(:,1))./sqrt(sum(Mtrue(:,1).^2).*sum(Msisal(:,1).^2));
SISAL_MAX_ANG = acos(min(angles(:)))*180/pi;
End

2.5. CoNMF algorithm

CoNMF is used with another regularization term to promote minimum volume by pushing the endmembers toward the mean value of the data set or bring the endmembers to the real solution quadratically regularized by a given simplex, other than the minimum volume [12, 13]. CoNMF does not require a prior step to estimate the number of endmembers and can be effectively used in scenarios in which the number of endmembers is not known a priori [29].

Input : (dataset), T ∈ N a > 0, β > 0 (regularization parameters) q > p (overestimate sequence of parameters) δ(stopping threshold), θ (a very small number) Output : (M, S) (M represent mixing and abundances) Initialization /* overestimate the signal subspace*/
U ∈ R^d×p ← Hysine(Y, q)/ * orthogonal basics*/ Y ← U^TY; Y ← Y/ ||Y||
V ← orth(Y*ỹ/||ỹ||;q-1)/ * q principal components */ A(0) ← VCA(Y, q)/ * estimate q endmembers */
A(0) ← V^T(A(0) − Y)
P ← A(0)/ * the VCA solution is used as pure pixel */
X(0) ← SoftSAL(A(0), Y)/ * abundances */
ε₀ = 0; t ← 0
Begin
Repeat
\[ t \Rightarrow t+1 \ (\text{optimize with respect to } A) \]
\[ \Delta A_{t-1} \Rightarrow V^T((Y - \hat{Y})X_{t-1}^T + \beta(P - \tilde{P}) + \beta A_{t-1})(X_{t-1}X_{t-1}^T + (\beta - A_{t-1})I) \]
\[ A_{t+1} \Rightarrow \hat{Y} + \beta \Delta A_{t-1} \] (optimize with respect to X)
\[ Y' \Rightarrow [V^T \sqrt{\mu A_{t+1}}] \]
\[ A_{t+1} \equiv [A_{t+1}^T \mu_{t}]^T \]
End
In this paper, the USGS library for mineral is used as ground truth for real endmember that contain 5 endmembers as reference. The database for algorithm is taken from previous paper [7, 8, 10, 12]. It is then generated in Matlab 2019 software on Acer Swift SF314-41 with AMD Ryzen 5 3500U with Radeon Vega Mobile Gfx 2.10GHz processor, 64-bit operating system type, with 8Gb RAM.

3. RESULTS AND ANALYSIS

The SAD is used to evaluate the performance of estimated endmembers, which is an angle distance between an estimated endmember and its corresponding ground truth. It defined as:

\[ SAD(m, \hat{m}) = \arccos\left(\frac{m^T \hat{m}}{\|m\| \|\hat{m}\|}\right) \]  

(1)

where m denotes the ground truth of one endmember, while \( \hat{m} \) represent the corresponding estimated results. The smaller SAD corresponds to a better performance. One of the main aspects in this project is the unmixing process of the proposed compared algorithms. Figure 3 show the comparison of five endmember of spectral signature with respect to the endmember extraction by four algorithms. The material for these five endmember is tabulated in Table 1. From Figure 3, the dotted line is true spectral signature from library spectral compared purple line extracted by CoNMF algorithm, red line is extracted by NFINDR algorithm, green line is extracted by VCA algorithm and the last one blue line is extracted by SISAL algorithm. The entire algorithm using same data but different technique of extraction of endmembers. Hence, all algorithm demonstrates excellent extraction by resulting the spectral signature almost exactly same with spectral library.

Figure 3. Comparison of the five spectral signatures in cuprite scene with different algorithms.

| Table 1. Reference spectral signature |
|--------------------------------------|
| Endmember 1 | #6 kaolinite |
| Endmember 2 | #10 pyrope |
| Endmember 3 | #8 montmorillonite |
| Endmember 4 | #5 kaolinite |
| Endmember 5 | #12 chalcedony |

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The first experiment aims to investigate the best spectral angle distance estimated by four difference algorithms. Table 2 point out the difference performance of spectral angle distance estimated by four difference algorithms with different noise level. The first column of table show the noise level that was used. The four left columns list the spectral angle distance difference between estimated difference algorithms. At noise level is 30 db, the SAD for CoNMF is 0.619155, SAD for VCA is 0.890067, SAD for NFINDR is 0.847781 and SAD for SISAL is 2.568448, which is CoNMF algorithm is smaller than other and show best performance. But, it difference with using noise level 40 db, the value SAD for all algorithms drop more smaller than using 30 db. The SAD for CoNMF is 0.495250, SAD for VCA and NFINDR is 0.552555, and SAD for SISAL is 0.727632. The third noise level is 60db, The SAD for CoNMF is 0.552818, SAD for VCA and NFINDR is 0.659840, and SAD for SISAL is 0.023277.

Table 2. SAD and different noise level with SNR value 30 dB, 40 dB, 60dB

| SNR | Algorithm (SAD) | CoNMF | VCA | NFINDR | SISAL |
|-----|----------------|-------|-----|--------|-------|
| 30  | 0.619155       | 0.890067 | 0.847781 | 2.568448 |
| 40  | 0.495250       | 0.552555 | 0.552555 | 0.727632 |
| 60  | 0.552818       | 0.659840 | 0.659840 | 0.023277 |

The second experiment aims to measure the spectral angle distance for each endmember by the noise level for 30db and 40dB. Table 3 shows the result of the experiment. The results proves that the SAD for endmember 1 extracted by CoNMF algorithms is archived 100% similar with the original endmember. Besides, the SAD for endmember 3 extracted by SISAL algorithm show smaller than extracted CoNMF algorithm. If the smaller SAD, better performance of unmixing process.

Table 3. SAD between five endmember for SNR 30dB and 40dB

| Endmember | SNR (30) | Algorithm (SAD) | CoNMF | VCA | NFINDR | SISAL |
|-----------|---------|----------------|-------|-----|--------|-------|
| Endmember 1 | 0.000000 | 0.356500 | 0.356500 | 1.127762 |
| Endmember 2 | 0.404453 | 0.802739 | 0.802739 | 2.072371 |
| Endmember 3 | 0.493473 | 0.646359 | 0.231876 | 0.231876 |
| Endmember 4 | 0.619155 | 0.839424 | 0.839424 | 1.127762 |
| Endmember 5 | 0.180157 | 1.633885 | 0.506502 | 0.890067 |

| Endmember | SNR (40) | Algorithm (SAD) | CoNMF | VCA | NFINDR | SISAL |
|-----------|---------|----------------|-------|-----|--------|-------|
| Endmember 1 | 0.000000 | 0.476512 | 0.476512 | 0.324057 |
| Endmember 2 | 0.438316 | 0.530236 | 0.530236 | 0.631297 |
| Endmember 3 | 0.249520 | 0.552555 | 0.552555 | 0.727632 |
| Endmember 4 | 0.495250 | 0.013281 | 0.598216 | 0.598216 |
| Endmember 5 | 0.188265 | 0.337724 | 0.337724 | 0.540945 |

The next experiment aims to measure the spectral angle distance for each endmember by the noise level 60 dB. Table 4 shows the result of the experiment. The results proves that the SAD for endmember 1 extracted by CoNMF algorithms is archived 100% similar with the original endmember and extracted by SISAL algorithm exactly similar to the real ones. Besides, the SAD for endmember 2 and 3 extracted by SISAL algorithm show smaller than extracted CoNMF algorithm. But the SAD for endmember 4 and 5 is extracted by VCA algorithm show smaller other and better performance than other algorithms. If the smaller SAD, better performance of unmixing process.

For illustrative purpose, Figure 4 show the comparison of the real endmember with estimate endmember extracted with different algorithm but resulting same spectral signature. The SNR used is 40 dB as it shows the best result compared to the other algorithms. This estimation obtained on real data in absence of pure pixel. The SAD for endmember is calculated based on estimated endmember and true endmember. The result shows the estimated signature by CoNMF are similar to the real ones, whereas the other algorithm is slightly different. This experiment show that CoNMF is the best algorithm to be used in hyperspectral unmixing other than the other three algorithms.

Table 4. SAD between five endmember for SNR 60dB

| Endmember | SNR (60) | Algorithm (SAD) | CoNMF | VCA | NFINDR | SISAL |
|-----------|---------|----------------|-------|-----|--------|-------|
| Endmember 1 | 0.000000 | 0.588549 | 0.588549 | 0.002067 |
| Endmember 2 | 0.326088 | 0.533598 | 0.533598 | 0.023277 |
| Endmember 3 | 0.493473 | 0.231876 | 0.231876 | 0.013281 |
| Endmember 4 | 0.180157 | 1.633885 | 0.506502 | 0.890067 |
| Endmember 5 | 0.506061 | 0.011777 | 0.659840 | 0.659840 |
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4. CONCLUSION

Four major algorithms on unmixing approaches CoNMF, VCA, NFINDR, and SISAL have been studied. The results are compared between each algorithms based on the SAD value of spectral signature. Under different noise levels, when the noise level is moderately low at 40 dB, the algorithms can obtain very good unmixing results. In turn, when SNR larger than or smaller than 40 dB, the quality of the unmixing result decrease particularly regard to the SAD value. However, the SNR start with 30 dB because 20 dB is not realistic noise level for imaging spectrometer. As a result, it can conclude that 40 dB indicate very high robustness to noise by algorithms, and CoNMF is the best algorithm to be used on unmixing approach compared to the other algorithms.

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Figure 4. Comparison each endmember for different algorithm with snr 40 dB
Ain Zat Mohd Yusof received his Bachelor’s degree in Electronic and Computer engineering from Technical University of Malaysia Malacca in 2016. Since 2018, he has been pursuing his Master’s degree in the same university, majoring in Signal Processing. His research interest include multispectral imaging, hyperspectral imaging, and spatial and spectral constraint.
Redzuan Abdul Manap received the BEng degree in electrical and electronic engineering from The University of Nottingham, UK in 2002, the MSc degree in communication and signal processing from University of Newcastle upon Tyne, UK in 2004 and the PhD degree in electronic engineering from The University of Sheffield, UK in 2018. He is currently a Senior Lecturer at Faculty of Electronics and Computer Engineering, Universiti Teknikal Malaysia Melaka (UTeM), Malaysia. His research interests include image processing, visual perception, machine learning and computer vision. He has published around 20 journals and proceeding papers in these areas.

Abd Majid Darsono was born in Malaysia in 1980. He received the Bachelor degree in communication and computer engineering from Universiti Kebangsaan Malaysia in 2002 and the MSc degree in electronic communications and computer engineering from The University of Nottingham, United Kingdom in 2005. In 2012, he received the Ph.D. degree in signal processing from University of Newcastle upon Tyne, United Kingdom. He joined Universiti Teknikal Malaysia Melaka (UTeM) since 2005 as a lecturer. He is currently an Associate Professor in Faculty of Electronics and Computer Engineering in UTeM. His research experience and interests include statistical signal processing, and speech and image processing.