Highly efficient carrier multiplication in PbS nanosheets

Michiel Aerts¹, Thomas Bielewicz², Christian Klinke², Ferdinand C. Grozema¹, Arjan J. Houtepen¹, Juleon M. Schins¹ & Laurens D.A. Siebbeles¹

Semiconductor nanocrystals are promising for use in cheap and highly efficient solar cells. A high efficiency can be achieved by carrier multiplication (CM), which yields multiple electron-hole pairs for a single absorbed photon. Lead chalcogenide nanocrystals are of specific interest, since their band gap can be tuned to be optimal to exploit CM in solar cells. Interestingly, for a given photon energy CM is more efficient in bulk PbS and PbSe, which has been attributed to the higher density of states. Unfortunately, these bulk materials are not useful for solar cells due to their low band gap. Here we demonstrate that two-dimensional PbS nanosheets combine the band gap of a confined system with the high CM efficiency of bulk. Interestingly, in thin PbS nanosheets virtually the entire excess photon energy above the CM threshold is used for CM, in contrast to quantum dots, nanorods and bulk lead chalcogenide materials.
n semiconductors, photoexcitation leads to formation of an electron in a conduction band state and a hole in a valence band state. The electron–hole (e–h) pair initially has an excess energy equal to the difference between the photon energy and the band gap. The charges can lose their excess energy by cooling to states at the band edge via electron–phonon scattering. A hot charge carrier with excess energy larger than the band gap may also relax by exciting another electron across the band gap. The latter process is known as carrier multiplication (CM): the transition from a hot charge carrier state to an energetically equivalent trion state. The trion consists of a charge carrier at lower energy and an additional e–h pair. CM competes with electron–phonon scattering until the hot charge carrier has cooled below the CM threshold. The competition between CM and inelastic electron–phonon scattering determines the final number of e–h pairs that are produced. The quantum yield of CM is defined as the number of e–h pairs produced per absorbed photon. An e–h pair in a trion can recombinates by transferring the excitation energy to the third charge. This process is the inverse of Auger recombination. In strongly confined e–h pairs, Coulomb interactions are enhanced with respect to bulk, leading to an increased coupling between a single hot carrier and a trion. This makes carrier–trion interconversion processes much more efficient in confined structures than in bulk semiconductors.

Much attention has been paid to how nanocrystal shape affects CM. The extent to which a hot charge carrier undergoes the CM process is determined by the following factors: first, the Coulomb coupling strength between the hot charge and the equally energetic trion, which also depends on the dielectric constant of the environment; second, the density of final trion states that are coupled to the initial hot charge carrier state; and third, the dephasing between the hot charge carrier state and the trion states. The influence of all these factors on the CM process, as well as on the competing decay of hot charge carriers by electron–phonon cooling, varies with nanocrystal dimensionality and size. The demonstration of CM in quantum dots and nanorods of lead chalcogenides is of interest, since their dimensionality and size. The demonstration of CM in quantum dots and nanorods of lead chalcogenides is of interest, since their dimensionality and size.

In this Article, we show that for thin PbS nanosheets of 4 nm thickness, the photon energy in excess of the CM threshold is 3 eV. The absorption threshold of the nanosheets is blue-shifted with respect to bulk, and in the range 4–7 nm is near 3 eV.

**Results**

**Synthesis and structural characterization.** PbS nanosheets, passivated by an oleic acid ligand layer, were synthesized according to a recently developed method. Thin-film samples were prepared by drop-casting the nanosheets from toluene onto a quartz substrate. Details on the synthesis can be found in the Methods section. The nanosheet thickness as obtained from X-ray diffraction through the Scherrer equation is 3 ± 1, 5 ± 1 and 6 ± 1 nm) is close to that obtained from X-ray diffraction through the Scherrer equation (4.0 ± 0.1, 5.9 ± 0.1, 7.0 ± 0.1 nm, respectively). Supplementary Fig. 1 shows representative transmission electron microscopy and AFM images of nanosheets. In this Letter we refer to the thickness as obtained from the X-ray diffraction measurements.

The absorption threshold of the nanosheets is blue-shifted with respect to bulk, and in the range 4–7 nm is near 3 eV.
the analytical solution to the differential equation for first- and second-order decay, \((dn)/(dt) = -k_n - k_2 n^2\), with \(n\) the (e–h) pair density, \(k_1 = 1.1\) ns\(^{-1}\) the first-order decay rate and \(k_2 = 2.5 \times 10^{-22}\) cm\(^3\) ps\(^{-1}\) the second-order Auger recombination rate.

The high quality of the global fit (hardly discernible from the experimental data) shows that Auger recombination follows second-order decay kinetics, which is typical for tightly bound e–h pairs that move together in the form of neutral excitons\(^{24,25}\). In the PbS dimensional extremes of 3D bulk and 0D quantum dots, electrons and holes do not pair up, and therefore decay via third-order Auger recombination\(^{24}\).

### Determination of quantum yield

The maximum in the transient bleach, occurring at 3 ps after photoexcitation (corresponding to the cooling time of hot excitons), increases linearly with the absorbed pump laser fluence, or equivalently the exciton density, if higher-order Auger recombination is insignificant on this timescale. In the latter case, the exciton density can be determined from the maximum transient bleach, similar to previous transient terahertz conductivity measurements on bulk PbS and PbSe\(^{18}\), and time-resolved microwave conductivity measurements on PbSe QD films\(^{26}\).

Figure 3 shows the maximum transient bleach signal \(\Delta T_{\text{max}}/T\) for various pump laser fluences and photon energies for the 5.9 nm thick PbS nanosheets. Similar data for the other nanosheet samples are shown in Supplementary Fig. 2 (4 nm thickness) and Supplementary Fig. 3 (7 nm thickness). The linear increase in \(\Delta T_{\text{max}}/T\) with pump fluence reflects that the maximum in the transient bleach is directly proportional to the density of excitons and that higher-order exciton decay is negligible during the first 3 ps after the pump pulse. The relative uncertainty in \(\Delta T_{\text{max}}/T\) is determined by the noise in transients as those in Fig. 2, and amounts to 1%. The maximum transient bleach signal \(\Delta T_{\text{max}}/T\) depends linearly on the number of e–h pairs absorbed per photon (that is, the quantum yield, \(\Phi\)), the pump photon fluence, \(I_0\), and the fraction absorbed pump photons, \(F_A\), according to

\[
\Delta T_{\text{max}}/T = \Phi \sigma_{TB} I_0 F_A
\]

The value of transient bleach cross-section \(\sigma_{TB} = 1.7 \pm 0.1 \times 10^{-15}\) cm\(^2\) was determined from the value of \(\Delta T_{\text{max}}/T\) obtained by photoexcitation with a known number of absorbed photons per unit area, \(I_0 F_A\), at low photon energy of 0.95 eV for which CM is energetically impossible and hence \(\Phi = 1\). Note that the transient bleach cross-section \(\sigma_{TB}\) is not to be identified with the steady-state absorption cross-section (in the case of negligible spectator shift the latter is a factor \(\gamma/2\) larger, with \(\gamma\) being the degeneracy of the band edge exciton)\(^{27}\). From equation 1 it follows that the derivative of \(\Delta T_{\text{max}}/T\) versus \(I_0 F_A\) scales with the quantum yield \(\Phi\). The three lowest pump photon energies coincide on a unique line characterized by unit quantum yield. The slope increases for the highest three pump photon energies, implying an increasing quantum yield, reaching a quantum yield of up to 2.2 after exciting with 4.66 eV pump photons. Numerical values of the quantum yield are given in the legend of Fig. 3.

### Discussion of CM efficiency

Figure 4a shows a plot of the quantum yield \(\Phi\) versus pump photon energy \(h\nu\) for three PbS nanosheet samples; that is, for each nanosheet a fluence set of data as in Fig. 3 is converted to a single data point in Fig. 4. The relative uncertainty in the quantum yields in Fig. 4 is at most 8% and is because of the uncertainty in the fraction of pump light absorbed, \(F_A(2\%)\), the noise in the photobleaching transients \(\Delta T_{\text{max}}/T\) (1%) and the incident pump fluence, \(I_0(5\%)\)—see Methods section. In addition, displayed in the figure are recent literature data on PbS quantum dots\(^{12,13}\) and bulk PbS\(^{18}\). For the quantum dots, care was taken to select only data from experiments that were properly flowed or stirred, to avoid artificially high quantum yields or low thresholds for CM\(^{28}\). Interestingly, the CM threshold has the same value of \(h\nu_{\text{th}} = 3\) eV for the three nanosheet samples, despite the different thickness and band gap. This threshold is similar to that reported for PbS quantum dots, which after conversion to photon energy are found to be near 3 eV\(^{12,13}\). This threshold is significantly higher than in bulk PbS (\(h\nu_{\text{th}} \approx 23) eV\(^{18}\). Further studies are needed to elucidate why the threshold for bulk differs from that of nanocrystals, for which the threshold does not depend on dimensionality or size. Above the threshold, the quantum yield for PbS nanosheets increases with photon energy as \(0.95 \pm 0.15\) eV\(^{-1}\). This CM efficiency (that is, \(d\Phi/d(h\nu)\)) is comparable to bulk PbS and is significantly higher than that for PbS quantum dots (\(0.3\) eV\(^{-1}\))\(^{12,17,18}\). We believe that the dimensional trends of...
Quantum yield \( \Phi \) plotted versus (a) pump photon energy \( h\nu \), or (b) band gap multiple \( h\nu/E_g \) for PbS nanosheets with thicknesses as indicated. The uncertainties in the quantum yields have been determined as described in the text and in the Methods section. In addition displayed is recent literature data on obtained quantum yields in PbS bulk and quantum dots. In b the slope of the data points is equal to the CM efficiency \( \eta_{cm} \) (solid lines).

CM threshold and CM efficiency have their origin in the band structure and the influence of quantum confinement on the discretization of wave vectors. Above the CM threshold, the efficiency of CM we find for two-dimensional (2D) nanosheets is similar to bulk, and much higher than for quantum dots and rods. This might be related to the fact that the discretization of wave vector states in confined systems severely limits the available trion states that can couple to the hot exciton. It appears that 2D nanosheets provide an optimum combination of an enhanced band gap due to quantum confinement perpendicular to the plane of the sheet with a high density of states due to spatial extent of electronic states in the plane of the sheet.

For solar cell applications, the number of e–h pairs produced per unit photon energy normalized to the band gap \( E_g \) is usually considered as the appropriate measure of CM efficiency. According to this, the normalized CM efficiency is \( \eta_{cm} = E_g (d\Phi)/d(h\nu) \). Figure 4b shows the quantum yield versus the photon energy normalized to the band gap, together with the values of \( \eta_{cm} \) obtained from the slopes of linear fits to the data above the CM threshold. The normalized CM efficiencies range from \( \eta_{cm} = 0.9 \pm 0.15 \) for the thinnest nanosheets \((d = 4 \text{ nm})\) to \( \eta_{cm} = 0.55 \pm 0.10 \) for the thicker nanosheets. For the thinnest nanosheets, \( \eta_{cm} \) is close to 1, which implies that virtually all photon energy in excess of the CM threshold is converted into additional e–h pairs. The value for the thinnest nanosheets is significantly higher than the results for \( \eta_{cm} \) in lead chalcogenide quantum dots, nanorods and bulk, which are in the range \( 0.3–0.5 \).

The normalized CM efficiency in 2D PbS nanosheets is higher than previously published results for 0D quantum dots, 1D nanorods and 3D bulk. In 4 nm thick PbS nanosheets, almost all photon energy in excess of the CM threshold is converted into additional e–h pairs. The CM threshold near 3 eV in PbS nanosheets is similar to that for quantum dots. It should be noted, however, that the fraction of solar photons with energy above this threshold energy is small. This makes these nanosheets of limited practical use for exploitation of CM in solar cells. Further studies are needed to combine the near maximum CM efficiency in 2D nanosheets with a lower threshold energy.

**Methods**

**Synthesis of PbS nanosheets.** The PbS nanosheets were synthesized according to a previously published method. The procedures used in the synthesis were slightly varied in order to produce the three samples with different thicknesses. The 4 nm thick sheets were prepared by dissolving 860 mg of lead acetate in a mixture of 10 ml diphenyl ether, 0.1 ml trioctylphosphine and 2 ml oleic acid. The blend was heated under \( N_2 \) atmosphere to 85°C and degassed. Then, the mixture was heated to 130°C and 1 ml 1,1,2-trichloroethane was added rapidly at 100°C before reaching 130°C. 1.4 mg thioacetamide was added in 0.23 ml dimethylformamide to start the reaction. The 5.9 nm thick sheets were prepared by dissolving 860 mg of lead acetate in a mixture of 10 ml diphenyl ether and 3.5 ml oleic acid. The blend was heated under \( N_2 \) atmosphere to 85°C and degassed. Then, the mixture was heated to 160°C and 1 ml 1,1,2-trichloroethane was added rapidly at 100°C, and before reaching 160°C 1.4 mg thioacetamide was added in 0.23 ml dimethylformamide to start the reaction. The 7 nm thick sheets were prepared by dissolving 860 mg of lead acetate in a mixture of 10 ml diphenyl ether and 3.5 ml oleic acid. The blend was heated under \( N_2 \) atmosphere to 85°C and degassed. Then, the mixture was heated to 160°C and 1 ml 1,1,2-trichloroethane was added rapidly at 100°C, and before reaching 160°C 1.4 ml of thioacetamide in 0.2 ml dimethylformamide were added to start the reaction. For all three syntheses, after 5 min the synthesis mixture was slowly cooled down to room temperature and centrifuged. The residue was washed twice with toluene and the final nanosheet product was finally suspended in toluene.

**Nanosheet characterization.** The nanosheets were characterized by transmission electron microscopy (JEOL Jem-1011). X-ray diffraction (Philips X’Pert System with a Bragg-Brentano geometry and a Cu K-alpha X-ray with a wavelength of 0.154 nm) and AFM (Veeco Dimension 3100). For the optical measurements, the nanosheets were drop-casted from toluene on a quartz substrate. The quartz was functionalized via silanization in order to provide better adherence of the nano-crystals, as has been described previously. All optical measurements were performed without exposing the samples to air, by using air-tight sample holders that were loaded inside a nitrogen-filled glovebox. The absorption spectra of the samples were measured with a Perkin Elmer Lambda 900 spectrophotometer, equipped with an integrating sphere. The sample was placed inside the integrating sphere, so that light scattered from the sample also enters the photodetector. Background absorption of the quartz substrate was subtracted. The relative uncertainty in the fraction of absorbed light is 2%, which was statistically determined via repeated measurements.

**Transient absorption setup.** The dynamics of photogenerated electrons and holes was measured with two different time-resolved laser pump-probe optical absorption facilities. The thicker nanosheets \( (d = 5.9 \text{ nm and } 7.0 \text{ nm}) \) were excited and probed by <100-fs pulses from a 1.5-kHz Ti:sapphire ultrastable amplifier laser system (Libra, Coherent), either directly, after frequency-doubling or -tripling, or after optical parametric amplification (OPera and TOPAS, Coherent). The pump laser fluence was varied using neutral density filters. The pump fluence \( I_0 \) was determined as the maximum power passing through a 3-mm pinhole at the position of the sample. Repeated measurements of \( I_0 \) yielded a spread of 5%. The pump-induced transient bleach signal near the band gap was measured on balanced InGaAs photodiodes (Hamamatsu). The thin nanosheets \( (d = 4.0 \text{ nm}) \) were excited with ~200-fs laser pulses (Light Conversion Pharos-SP combined with Orpheus OPA) and probed using multichannel detection of near-infrared (1,080–1,630 nm) probe pulses (Ultrastable Systems Helios), which were generated by focusing 1,030 nm light in a sapphire crystal. The overlap between the pump beam (diameter 6–7 mm) and probe beam (diameter 1 mm) was optimized by...
maximizing the amplitude of the transient photobleach signal \( \Delta T/T \). The uncertainty in \( \Delta T/T \) is determined by the noise in transients as those in Fig. 2, and amounts to 1%.

References

1. Beard, M. C., Luther, J. M., Semonin, O. E. & Nozik, A. J. Third generation photovoltaics based on multiple exciton generation in quantum confined semiconductor dots. Nature 503, 454–458 (2013).

2. Shabaev, A., Efros, A. L. & Nozik, A. J. Multiexciton generation by a single photon in nanocrystals. Acc. Chem. Res. 46, 1261–1269 (2013).

3. Bartnik, A. C., Efros, A. L., Koh, W. K., Murray, C. B. & Wise, F. W. Electronic and optical properties of PbSe nanorods and nanowires. Phys. Rev. B 82, 195313 (2010).

4. Achstein, A. W. et al. Electronic structure and exciton-phonon interaction in two-dimensional colloidal CdSe nanosheets. Nano. Lett. 12, 3151–3157 (2012).

5. Jaeger, H. M., Hyeon-Deuk, K. & Prezhdo, O. V. Exciton multiplication from PbSe and PbS. Nano. Lett. 8, 1280–1289 (2008).

6. Cunningham, P. D. et al. Carrier multiplication in semiconductor nanocrystals: influence of size, shape, and composition. Acc. Chem. Res. 46, 1261–1269 (2013).

7. Padilha, L. A. et al. Carrier multiplication in semiconductor nanocrystals: influence of size, shape, and composition. Acc. Chem. Res. 46, 1261–1269 (2013).

8. Achtstein, A. W. et al. Highly efficient multiple exciton generation in colloidal PbSe and PbS quantum dots. Nano. Lett. 8, 865–871 (2008).

9. Mudgett, A. G. et al. Size and composition dependent multiple exciton generation efficiency in PbS, PbSe, and PbS,Se alloys. Nano. Lett. 13, 3078–3085 (2013).

10. Hardman, S. J. O. et al. Electronic and surface properties of PbS nanoparticles exhibiting efficient multiple exciton generation. Phys. Chem. Chem. Phys. 13, 20275–20283 (2011).

11. Nootz, G. et al. Size dependence of carrier dynamics and carrier multiplication in PbS quantum dots. Phys. Rev. B 83, 155302 (2011).

12. Cunningham, P. D. et al. Enhanced multiple exciton generation in quasi-one-dimensional semiconductors. Nano. Lett. 11, 3476–3481 (2011).

13. Cunningham, P. D. et al. Correction to enhanced multiple exciton generation in quasi-one-dimensional semiconductors. Nano. Lett. 13, 3003–3003 (2013).

14. Padilha, L. A. et al. Aspect ratio dependence of auger recombination and carrier multiplication in PbSe nanorods. Nano. Lett. 13, 1092–1099 (2013).

15. Pijpers, J. J. H. et al. Assessment of carrier-multiplication efficiency in bulk PbSe and PbS. Nat. Phys. 5, 811–814 (2009).

16. Schliehe, C. et al. Ultrathin PbS sheets by two-dimensional oriented attachment. Science 329, 550–553 (2010).

17. Scanlon, W. W. Recent advances in the optical and electronic properties of PbS, PbSe, PbTe and their alloys. J. Phys. Chem. Solids 8, 423–428 (1959).

18. Koh, S. E. et al. Electronic band-structure and optical properties of PbTe, PbSe, and PbS. Phys. Rev. B 8, 1477–1488 (1973).

19. Allan, G. & Delerue, C. Confinement effects in PbSe quantum wells and nanocrystals. Phys. Rev. B 70, 245321 (2004).

20. Moreels, P. et al. Size-dependent optical properties of colloidal PbS quantum dots. ACS Nano. 3, 3023–3030 (2009).

21. Aerts, M. et al. Cooling and Auger recombination of charges in PbSe nanorods: crossover from cubic to bimolecular decay. Nano. Lett. 13, 4380–4386 (2013).

22. Kunneman, L. T. et al. Bimolecular Auger recombination of electron–hole pairs in two-dimensional CdSe and CdSe/CdZnS core/shell nanoplatelets. J. Phys. Chem. Lett. 4, 3574–3578 (2013).

23. Aerts, M. et al. Free charges produced by carrier multiplication in strongly coupled PbSe quantum dot films. Nano. Lett. 11, 4485–4489 (2011).

24. Trinh, M. T. et al. In spite of recent doubts carrier multiplication does occur in PbSe nanocrystals. Nano. Lett. 8, 1713–1718 (2008).

25. McGuire, J. A., Sykora, M., Joo, J., Pietryga, J. M. & Klimov, V. I. Apparent versus true carrier multiplication yields in semiconductor nanocrystals. Nano. Lett. 10, 2049–2057 (2010).

26. Beard, M. C. et al. Comparing multiple exciton generation in quantum dots to impact ionization in bulk semiconductors: implications for enhancement of solar energy conversion. Nano. Lett. 10, 3019–3027 (2010).

Acknowledgements

M.A. acknowledges financial support for this research from ADEMA, A green Deal in Energy Materials of the Ministry of Economic Affairs of The Netherlands (www.adem-innovationlab.nl), T.B. and C.K. thank the European Research Council (Seventh Framework Program FP7, Project: ERC Starting Grant 2D-SYNTERA) for funding.

Author contributions

M.A. performed all the experiments. M.A., L.D.A.S. and J.M.S. wrote the manuscript and developed the underlying concepts. A.J.H. and F.C.G. facilitated the white light equipment. T.B. and C.K. developed the method of sample synthesis. T.B. synthesized and structurally characterized the samples. All authors read the manuscript and provided comments.

Additional information

Supplementary Information accompanies this paper at http://www.nature.com/naturecommunications

Competing financial interests: The authors declare no competing financial interests.

Reprints and permission information is available online at http://npg.nature.com/reprintsandpermissions/

How to cite this article: Aerts, M. et al. Highly efficient carrier multiplication in PbS nanocrystals. Nat. Commun. 5:3789 doi: 10.1038/ncomms4789 (2014).

This work is licensed under a Creative Commons Attribution-NonCommercial-NoDerivs 3.0 Unported License. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in the credit line; if the material is not included under the Creative Commons license, users will need to obtain permission from the license holder to reproduce the material. To view a copy of this license, visit http://creativecommons.org/licenses/by-nc-nd/3.0/