Lepton Number Violation and the Baryon Asymmetry of the Universe

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Neutrinoless double beta decay, lepton number violating collider processes and the Baryon Asymmetry of the Universe (BAU) are intimately related. In particular lepton number violating processes at low energies in combination with sphaleron transitions will typically erase any pre-existing baryon asymmetry of the Universe. In this contribution we briefly review the tight connection between neutrinoless double beta decay, lepton number violating processes at the LHC and constraints from successful baryogenesis. We argue that far-reaching conclusions can be drawn unless the baryon asymmetry is stabilized via some newly introduced mechanism.

Keywords: Lepton Number Violation, Baryogenesis, Neutrinos
1. Introduction

The discovery of neutrino masses is typically understood as a hint for physics beyond the Standard Model (SM). Intimately related to this link is the question whether lepton number is conserved or broken. After all, neutrino masses can be realized in two different ways, either as Majorana masses $\nu^c_L \nu_L$ or as Dirac masses $\nu^c_R \nu_R + \nu^c_L \nu_L$. In the first case, lepton number is broken. In the latter case the newly introduced right-handed neutrino is an SM singlet so that a Majorana mass $\nu^c_R \nu_R$ is allowed by the SM symmetry. So either lepton number is broken again or this operator has to be forbidden by a new symmetry. In this sense the problem how neutrino masses are related to physics beyond the Standard Model boils down to the question whether the accidental lepton number conservation in the Standard Model is enforced by a new symmetry or violated by LNV operators.

LNV can be searched for directly for example in neutrinoless double beta decay or at colliders. Moreover, lepton number violating interactions can be important in cosmology where they can both wash out or create the baryon asymmetry of the Universe (BAU). These apparently different phenomena are thus closely related (see Fig. 1) as will be discussed in the following.

![Diagram](https://via.placeholder.com/150)

**Fig. 1.** Neutrinoless double beta decay, lepton number violating processes at the LHC and the generation and survival of the Baryon Asymmetry of the Universe are closely interrelated.

2. Probing Lepton Number Violation with Neutrinoless Double Beta Decay

A sensitive probe of low energy lepton number violation is neutrinoless double beta decay ($0\nu\beta\beta$), the simultaneous transition of two neutrons into two protons and two electrons, without emission of any anti-neutrinos:

$$2n \rightarrow 2p + 2e^-.$$  (1)
While the most prominent decay mode is triggered by a massive Majorana neutrino being exchanged between Standard Model (SM) $V - A$ vertices, providing a bound on the effective Majorana neutrinos mass

$$\langle m_\nu \rangle = \sum_j U^2_{ej} m_j \equiv m_{ee},$$

in the sub-eV range, in principle any operator violating lepton number by two units and transforming two neutrons into two protons, two electrons and nothing else will induce the decay.

As discussed in detail in Refs. 4, 5, the most general operator triggering the decay can be parametrized in terms of effective couplings $\epsilon$ as shown in Fig. 2. The diagram depicts the exchange of a light Majorana neutrino between two SM vertices (contribution a), the exchange of a light Majorana neutrino between an SM vertex and an effective operator which is pointlike at the nuclear Fermi momentum scale $O(100$ MeV) (contribution b) and a short-range contribution triggered by a single dimension 9 operator being pointlike at the Fermi momentum scale (contribution d). Contribution c) which contains two non-SM vertices can be neglected when compared to contribution b). The most general decay rate contains all combinations of leptonic and hadronic currents induced by the operators

$$O_{V,A} = \gamma^\mu (1 \mp \gamma_5), O_{S,P} = (1 \mp \gamma_5), O_{T_{L/R}} = \frac{i}{2} \left[ \gamma^\mu, \gamma^\nu \right](1 \mp \gamma_5),$$

allowed by Lorentz invariance.

Examples for contribution b) are the Leptoquark and SUSY accompanied decay modes, examples for contribution d) are decay modes where only SUSY particles or heavy neutrinos and gauge bosons in left-right-symmetric models are exchanged between the decaying nucleons, for a recent overview see Refs. 1. Present experiments have a sensitivity to the effective couplings of

$$\epsilon < (\text{few}) \times (10^{-7} - 10^{-10}).$$

For the $d = 9$ operator triggering the contribution d) it can be estimated that an observation of $0\nu\beta\beta$ decay with present-day experiments would involve TeV scale particles and thus would offer good chances to see new physics associated with LNV at the LHC. A crucial prerequisite for such a conclusion is of course a possibility to discriminate among the various mechanisms which may be responsible for the decay. This is a difficult task but may be possible at least for some of the mechanisms by observing neutrinoless double beta decay in multiple isotopes Refs. 6, 7, or by measuring the decay distribution, for example in the SuperNEMO experiment Refs. 8. Another possibility to discriminate between various short range contributions to neutrinoless double beta decay at the LHC itself is to identify the invariant mass peaks of particles produced resonantly in the intermediate state or to analyze the charge asymmetry between final states involving particles and/or anti-particles Refs. 9, 10.
3. Neutrinoless Double Beta Decay at the LHC

While neutrinoless double beta decay is the prime probe for massive Majorana neutrinos, lepton number violation in general can be searched for also in collider processes. Indeed, as has been discussed for example for the special cases of left-right symmetric models\textsuperscript{13,14} and $R$-parity violating supersymmetry\textsuperscript{11,12} the short range contribution d) can easily be crossed into a diagram with two quarks in the initial state where resonant production of a heavy particle leads to a same-sign dilepton signature plus two jets at the LHC, see Fig. 3. In order to discuss the LHC bounds in a model-independent way similar to the effective field theory approach of\textsuperscript{4,5}, it is necessary to specify, which particles are produced in the process which requires a decomposition of the $d=9$ operator. Such a decomposition has been worked out in\textsuperscript{15} where two different topologies (topology 1 with two fermions and a boson in the internal lines and topology 2 with an internal 3-boson-vertex) have been specified. This decomposition was applied to the LHC analogue of $0\nu\beta\beta$ decay and first results for topology 1 have been derived in\textsuperscript{9,10}. The conclusion reached was that with the exception of leptoquark exchange, the LHC was typically more sensitive than $0\nu\beta\beta$ decay on the short range operators. Thus one could infer that typically and with some exceptions

- Either an observation of $0\nu\beta\beta$ decay would imply an LHC signal of LNV as well. In turn, no sign of LNV at the LHC would exclude an observation of $0\nu\beta\beta$ decay.
- Or $0\nu\beta\beta$ decay would be triggered by a long-range mechanism a) or b).
4. Baryon Asymmetry Washout

An observation of lepton number violation at low energies has important consequences for a pre-existing lepton asymmetry in the Universe. For example, the prominent leptogenesis scenario for a generation of the baryon asymmetry of the Universe assumes a lepton number (or $B - L$) and CP asymmetry created in the decays of heavy Majorana neutrinos in the early Universe, which later on is converted into a baryon asymmetry by the non-perturbative $B + L$ violating sphaleron transitions present in the SM. Obviously, such a lepton asymmetry can be washed out by lepton number violating interactions, and indeed it has been pointed out that any observation of lepton number violation at the LHC will falsify high-scale leptogenesis.

The basic argument is that the observation of LNV at the LHC will yield a lower bound on the washout factor for the lepton asymmetry in the early Universe. It is easy to see that this argument can be extended even further:

Just like the combination of $B - L$ violating $\nu_R$ decays in leptogenesis with $B + L$ violating sphaleron processes can produce a baryon asymmetry, $B - L$ violation observed e.g. at the LHC or elsewhere in combination with $B + L$ violating sphaleron processes will lead to a washout of any pre-existing baryon asymmetry, irrespective of the concrete mechanism of baryogenesis.

Combining this argument with the results of other discussions above, one can argue that an observation of short-range $0\nu\beta\beta$ decay will typically imply that LNV processes should be detected at the LHC as well, and this in turn will falsify leptogenesis and in general any high-scale scenario of baryogenesis.

Indeed, such arguments are not new. They have been first discussed in earlier work and later on used e.g. to constrain neutrino Majorana masses, light lepton number violating sneutrinos or Majorana mass terms for 4th generation neutrino states. However, only quite recently it has been realized that the argument can be shown to apply for all short range contributions and also for the long-range contribution in Fig. 2. It has been shown that the $\Delta L = 2$ processes induced
by the operator $\mathcal{O}_D$ can be considered to be in equilibrium and the washout of the lepton asymmetry is effective if

$$\frac{\Gamma_W}{H} = c'_D \Lambda_D \left( \frac{T}{\Lambda_D} \right)^{2D - 9} \gtrsim 1,$$

(5)

where $\Lambda_D$ is the scale of the associated effective operator (assumed to be generated at tree level) from Eq. 3 and $c'_D$ being a prefactor of order $O(10^{-3} - 1)$. 

Thus the far-reaching and strong conclusion can be drawn that the observation of any new physics mechanism (i.e. not the mass mechanism) of neutrinoless double beta decay will typically exclude any high-scale generation of the baryon asymmetry of the Universe.

Even more recently further studies have been published which analyze the relation of lepton number violation and the Baryon Asymmetry of the Universe in concrete models such as left-right symmetry or low energy seesaw models\textsuperscript{23,24}.

5. Loopholes

Of course these arguments are rather general and various loopholes exist in specific models. These include:

- Scenarios where LNV is confined to a specific flavor sector only. For example, $0\nu\beta\beta$ decay probes $\Delta L_e = 2$ LNV, only. It may be possible for example that lepton number could still be conserved in the $\tau$ flavor which is not necessarily in equilibrium with the $e$ and $\mu$ flavors in the early Universe\textsuperscript{16}. It has been discussed in\textsuperscript{21}, however, that an observation of LFV decays such as $\tau \rightarrow \mu \gamma$ may require LFV couplings large enough to wash out such a flavor specific lepton asymmetry when combined with LNV observed in a different flavor sector. In Fig. 4, the temperature intervals are shown where two individual flavor number asymmetries are equilibrated by LFV processes. When this interval overlaps with the $\Delta L = 2$ washout interval of one net flavor number (i.e. electron number if $0\nu\beta\beta$ is observed), the net number of the other flavor will be efficiently washed out as well. As can be seen, if $\tau \rightarrow \ell \gamma$ or $\mu - e$ conversion in nuclei was observed, the involved flavors would be equilibrated around the same temperatures as the washout from the LNV operators.

- Models with hidden sectors, new symmetries and/or conserved charges may stabilize a baryon asymmetry against LNV washout as suggested for the example of hypercharge in\textsuperscript{22}.

- Lepton number may be broken at a scale below the electroweak phase transition where sphalerons are no longer active.

It should be realized though that in general an observation of low energy LNV would invalidate any high-scale generation of the baryon asymmetry and that the aforementioned protection mechanisms should be addressed explicitly in any model combining low-scale LNV with high-scale baryogenesis.
Fig. 4. Temperature intervals where the given LNV and LFV operators are in equilibrium, assumed that the corresponding process is observed at the current (future) experimental sensitivity. (From 21.)

6. Conclusions

By simply combining the arguments made above, we can conclude as follows:

If neutrinoless double beta decay is observed, it is:

- Either due to a long-range mechanism, e.g. a light Majorana neutrino mass.
- Or due to a short-range mechanism. In this case it is very probable that lepton number is observed at the LHC. This, however, implies that baryogenesis is a low-scale phenomenon which also may be observable at the LHC. In this case there thus may well be a “two-for-one” deal at the LHC.

If, on the other hand, the BAU is generated at a high-scale, there will be no lepton number violation at the LHC. If, in this case, neutrinoless double beta decay is observed, it thus will be typically due to a long-range mechanism. In combination with the assumption that we do not have a hint for lepton number violation at a low-scale in this case and on the other hand a mechanism for the generation of the BAU at a high-scale, this will probably point towards a high-scale origin of the neutrino mass as well, such as a vanilla-type seesaw mechanism in combination with leptogenesis.

Thus in summary an observation of neutrinoless double beta decay will typically (see Fig. 5)
High Scale Baryogenesis

LNV @ LHC

If 0vBB

Mass Mechanism

0vBB Decay

Mass Mechanism

New Physics

LNV @ LHC

Low Scale Baryogenesis

Very probably: High scale origin of $m_\nu$

Also detectable @ LHC?

"2 for 1"

Fig. 5. Conclusions as a logic tree: a discovery of lepton number violation at low energies will have far-reaching consequences for the origin of the Baryon Asymmetry of the Universe. On the other hand, if the Baryon Asymmetry is generated by a high-scale mechanism of baryogenesis interesting consequences for the search of low energy lepton number violation and the origin of neutrino masses can be deduced.

- *Either* imply LNV at the LHC and low-scale baryogenesis and thus a possible observation of both processes in the near future.
- *Or* very probably a high-scale origin of both neutrino masses and baryogenesis.

We thus think that even if possible loopholes to these arguments may exist, it is important to stress these relations to make both model builders and experimentalists aware of the tight connections between neutrinoless double beta decay, the search for lepton number violation et the LHC and the origin of the Baryon Asymmetry of the Universe.

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