MACE: Multi-Agent Autonomous Collaborative Exploration of Unknown Environments

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Abstract—In this paper, we propose a new framework for multi-agent collaborative exploration of unknown environments. The proposed method combines state-of-the-art algorithms in mapping, safe corridor generation and multi-agent planning. It first takes a volume that we want to explore, then proceeds to give the multiple agents different goals in order to explore a voxel grid of that volume. The exploration ends when all voxels are discovered as free or occupied, or there is no path found for the remaining undiscovered voxels. The state-of-the-art planning algorithm uses time-aware Safe Corridors to guarantee intra-agent collision safety as well safety from static obstacles. The presented approach is tested in a state of the art simulator for up to 4 agents.

video: https://youtu.be/v7P7HpBRY50

I. INTRODUCTION

A. Problem statement

Multi-agent exploration has numerous real world applications such as search and rescue, infrastructure inspection and cave exploration. An exploration framework that is computationally efficient and safe is thus tremendously beneficial. It is the purpose of this paper to present a new method for multi-agent exploration that is suitable for low compute embedded systems.

B. Related work

1) Single multirotor planning: Many works address single quadrotor planning. Recent state-of-the-art contributions use Safe Corridors to account for unknown/unexplored part of the environment and guarantee trajectory safety [1], [2]. Safe Corridors are a series of overlapping convex polyhedra that cover only free space and are used in many autonomous navigation methods [3] [4]. In [2], the authors use Safe Corridors in a MPC/MIQP formulation that is computationally efficient and accounts for drag forces. Our work is based on their approach with modifications to account for other moving agents.

2) Multi-agent planning: While some works have addressed multi-agent planning [5], [6], [7], [8], [9], [10], [11], only few works address the problem of low compute and safe multi-agent autonomous exploration while avoiding static obstacles and other exploring agents. In [12] the authors present an autonomous multi-agent planning solution using only on-board resources. The presented approach does not address full volume exploration and focuses only on intra-agent collision avoidance as well as static obstacle collision avoidance.

3) Exploration: Single quadrotor exploration and frontier analysis/selection has been extensively studied in the literature. Recent work [13] has shown significant improvement over other methods such as [14], [15], [16]. The proposed method uses a frontier information structure (FIS) that is maintained incrementally. It is provided to the exploration planner that plans exploration motions in three sequential steps: it first finds global tours that are efficient; then it selects a local set of optimal viewpoints; finally it generates minimum-time local trajectories. However, it is unclear how to scale this approach to multi-agent planning and whether the computational efficiency would be maintained. It is why we inspired our goal selection method from the Classical method [15] for frontier/goal selection, which scales well for multiple agents.

C. Contribution

The main contribution of our paper is a novel exploration framework that is based on a decentralized and synchronous planning method. The planning method takes inspiration mainly from [2] for single quadrotor planning and static obstacle avoidance, [10] for intra-agent collision avoidance, and [15] for goal selection for each agent. The framework also uses recent advances in state-of-the-art mapping [17] and Safe Corridor generation [18] [19] that makes it low compute and suitable for embedded systems. The planning framework is tested in simulation using the state-of-the-art Airsim [20] simulator.
D. Assumptions

The following assumptions are made:

- The position of each agent is known within a certain range of uncertainty. In the simulation, the position of each agent is known perfectly, but our framework can account for uncertainties by inflating each agent’s collision radius.
- All agents can communicate with each other within a certain delay. The communication only needs to happen when agents are close to each other.
- All agents can communicate with a central hub within a certain delay. The central hub will be tasked with merging each agent’s map with a global map and sending goals to each agent.

II. AGENT MODEL

| Symbol | Description                                      |
|--------|--------------------------------------------------|
| g      | gravity                                          |
| m      | multicopter mass                                 |
| p      | position vector $x, y, z$ in the world frame      |
| v      | velocity vector $v_x, v_y, v_z$ in the world frame|
| a      | acceleration vector from thrust and gravity in the world frame |
| j      | jerk vector $j_x, j_y, j_z$ in the world frame    |
| z_W    | world frame $z$                                  |
| z_B    | body frame $z$                                   |
| R      | rotation matrix from body to world frame         |
| D      | quadratic drag matrix                            |
| φ      | roll angle                                       |
| θ      | pitch angle                                      |
| ψ      | yaw angle                                        |
| c_cmd  | total thrust command                             |

Each agent is modeled after a multicopter whose control inputs are the attitude and thrust. The equations of motion are the following (nomenclature Tab. I):

\[
\begin{align*}
\dot{p} &= v \\
\dot{v} &= -gz_W + \frac{c_{cmd}}{m}z_B - RDR'v \|v\|_2 \\
\dot{\phi} &= \dot{\phi}_{cmd} \\
\dot{\theta} &= \dot{\theta}_{cmd} \\
\dot{\psi} &= \dot{\psi}_{cmd}
\end{align*}
\]

The above-mentioned equations are simplified into the following model:

\[
\begin{align*}
\dot{p} &= v \\
\dot{v} &= a - D_{lin,max}v \\
\dot{a} &= j
\end{align*}
\]

$D_{lin,max}$ is a diagonal matrix that represents the maximum linear drag coefficient in all directions. This matrix is identified offline as shown in [2]. The quadratic drag model is replaced with a linear worst-case scenario model. Many off-the-shelf solvers are very efficient for linear constraints, which is why we transformed the model into a linear one.

III. THE FRAMEWORK

The framework takes a volume that we want to explore, then proceeds to give all the agents different goals until all the volume is explored. The volume is represented as a voxel grid, and it is considered fully explored when all the voxels are either free or occupied, or no agent can find a path to the remaining unknown voxels. The framework is divided into 2 modules (Fig. 2).

1) A local module that is run on each agent and that contains mapping, planning and control submodules.
2) A global module that merges all the measurements of all the agents into a single global voxel grid. This module then sends goals to each agent to explore the volume.

Each of these modules as well as each submodule will be detailed separately in this section. We make the following assumptions:

1) The positions of all the agents are known within a certain range of uncertainty.
2) When the agents are close to each other they can communicate their positions and generated trajectories to each others within a certain delay.
3) The agents can all communicate with a central hub (running the global module) within a certain delay.

A. Local module - run on each agent

The local module is run on each agent and consists of 3 submodules: mapping, planning, and control.

1) Mapping: Each agent is equipped with an omnidirectional lidar that allows it to see in all directions. The output of the lidar is a pointcloud that is transformed into a voxel grid using a GPU accelerated method [17]. We remove the points associated to other agents appearing in the lidar scan.
This is done by removing all the points of the scan within a certain distance from the center of other agents (which we know due to the communication of trajectories between agents). The local voxel grid moves along with the agent such that the agent’s position is always in the center of the grid. Each voxel grid is sent to the global module to be merged into the global voxel grid.

2) Planning: Each agent plans locally to reach the goal sent to it by the global module. The planning framework is the same as [2], with modifications made to the Safe Corridor part to become time-aware as presented in [10]. This allows to avoid collision with other agents as well as static obstacles.

The planning framework is divided into the following steps that are executed sequentially and at a constant rate (Fig. 4):

1) Generate a global path that avoids static obstacles.
2) Generate a Safe Corridor.
3) Generate a time-aware Safe Corridor to avoid collision with other agents.
4) Generate a local reference trajectory using the global path and the the Safe Corridor.
5) Solve the MPC/MIQP problem to generate a trajectory close to the local reference trajectory and within the constraints of the time-aware Safe Corridor to guarantee safety.

First a global path is generated using Jump Point Search (JPS) [21] and Distance Map Planner (DMP) [22]. JPS is a shortest path algorithm that preserves A*’s optimality, while potentially lowering the computation time by an order of magnitude. The Distance Map Planner (DMP) [22] is used to make the generated path safer. It leverages the artificial potential field to push the path away from the obstacles (Fig. 3). We use the local voxel grid to search for the path. If the goal is outside the local voxel grid, an intermediate goal inside it is chosen as shown in [2].

Then, we create a Safe Corridor around that path to avoid static obstacles using the method described in [18]. The Safe Corridor covers only free voxels (unknown voxels are considered as obstacles). We only generate \( P_{hor} \) (polyhedra horizon used for optimization) overlapping polyhedra around the global path. \( P_{hor} \) is typically chosen equal to 2 to avoid high solving times.

Using the Safe Corridor (SC), we generate \( N \) local Safe Corridors \( SC_i, \ i = 1, 2, ..., N \) with \( N \) the number of discretization steps of the MPC/MIQP. Each \( SC_i \) is generated by adding the separating hyperplanes between the \( i \)th predicted position of the agent and the \( i \)th predicted position of all the other agents. These positions correspond to the solution of the MPC/MIQP at the last iteration. The generation of the \( SC_i \) is detailed in [10]. The series of \( SC_i \) is called time-aware SC.

We then generate a local reference trajectory \( x_{ref} \) by sampling the global path at a sampling velocity \( v_{samp} \) and sampling acceleration \( a_{samp} \) starting from the current agent position. These values are a user input but are usually chosen close to the agent dynamical limits. Any sampled point that is outside the SC is replaced by the most recent sampled point that is inside the SC. At each iteration, a new local reference trajectory is generated only if the predicted agent position \( x_N \) is within \( \text{thresh}_{dist} \) of \( x_{N,ref} \). More details about this step can be found in [2].

Finally, we use the time-aware SC and the local reference trajectory in a MIQP/MPC formulation to generate a trajectory that is safe from static obstacles and other moving agents. With \( \mathbf{x} = [p \ v \ a]^T, \ u = j, \ f(x(t), u(t)) \) defined by Eq. 6 the model is discretized using Euler to obtain the discrete dynamics \( x_{k+1} = f_d(x_k, u_k) \). The agent velocity is limited by the drag forces. The maximum bounds on the acceleration and the jerk in each direction are determined by the dynamics of the agent.

Collision avoidance is guaranteed by forcing every two consecutive discrete points \( k \) and \( k+1 \) (and thus the segment formed by them) to be in one of the overlapping polyhedra of a given local SC (\( SC_k \)). Let’s assume we have \( P \) overlapping polyhedra in \( SC_k \). They are described by \( \{(A_{kp}, c_{kp})\}, \ p = 0 : P - 1 \). The constraint that the discrete position \( p_k \) is in a polyhedron \( p \) is described by \( A_{kp} p_k \leq c_{kp} \). We introduce binary variables \( b_k \) (\( P \) variables for each \( x_k, k = 0 : N - 1 \) that indicate that \( p_k \) and \( p_{k+1} \) are in the polyhedron \( p \). We force all the segments to be in at least one of the polyhedra with the constraint \( \sum_{p=0}^{P-1} b_k \geq 1 \).

We formulate our MPC under the following Mixed-Integer Quadratic Program (MIQP) formulation. \( R_x, R_N \) and \( R_a \) are the weight matrix for the discrete state errors without the final state, the weight matrix for the final discrete state error (terminal state), and the weight matrix for the input,
Planning (run at a constant rate)

- Global Path Generator
- Safe Corridor Generator
- Local Reference Generator
- Time Aware SC Generator
- MIQP Solver

MIQP solution of other agents at the previous iteration

Fig. 4. We show the global pipeline of the planning framework of a single planning agent.

The MIQP is solved using the Gurobi solver [23].

3) Control: Each agent is controlled using a nonlinear MPC [24], with the acados toolkit [25]. The MPC minimizes the cost function:

\[
J = \int_0^T \left( \| x(t) - x_{ref}(t) \|^2_{Q_x} + \| u(t) - u_{ref}(t) \|^2_{R_u} \right) dt + \| x(T) - x_{ref}(T) \|^2_{Q_x}
\]

We use the model described in section with \( \mathbf{u} = [c_{cmd} \ \dot{c}_{cmd} \ \theta_{cmd} \ \dot{\theta}_{cmd}]^T \) and \( \mathbf{x} = [p \ \psi \ \theta \ \psi]^T \).

B. Global module - run on a central hub

This module takes a volume that we want to explore, merges the measurements/maps of all the agents, and sends a goal to each agent at a constant rate until that volume is fully explored. The volume is represented as a voxel grid and is considered fully explored when all the voxels are either free or occupied, or no agent can find a path to the remaining unknown voxels.

1) Merging maps from all agents: Each agent has its local voxel grid that is used for local obstacle avoidance and navigation. When this map is transmitted to the global module, we are able to efficiently merge it into the global map if the voxels of the local and global maps overlap with each others i.e. the vector formed by the origin of the local map and the origin of the global map has its \( x, y \) and \( z \) components as multiples of the voxel size. This can be achieved during the initialization phase, by setting the initial origin of all maps (local and global) to \((0, 0, 0)\). As presented in [17], the origin of the local voxel grid will be always offset in all directions by a multiple of the voxel size to keep the robot at its center.

We only update a voxel of the global grid if its corresponding voxel in the local voxel grid is free or occupied. In the case of static environments, we can add an additional condition to only update a voxel grid in a global grid if its not occupied (and its corresponding voxel in the local voxel grid is free or occupied).

2) Computing goals for agents: After updating the global map with the local voxel grids of all the agents, we proceed to compute goals for each agent. We define a neighbour voxel as a voxel that is reachable by moving at most 1 voxel unit in each direction from the current voxel. The goals are computed by doing the following steps sequentially (Fig. 5):

1) Find the border voxels: this is done by going over all the voxels of the global map. If a voxel is free and has a neighbour voxel that is unknown, then it is designated as a border voxel.

2) Cluster the border voxels: we form clusters out of the border voxels using the following rule: if two border voxel are neighbors, they belong to the same cluster.

3) Compute cluster centroid: we compute the centroid of each cluster by averaging the positions of all the voxels that belong to that cluster.

4) Compute potential goals: we compute potential goals by finding the voxel border in a cluster that is the closest to its centroid. If multiple voxels have the same closest distance, we chose one randomly.

5) Compute goals: the finals goals are computed by first choosing the closest potential goal to the first agent, and removing it from the potential goals’ list so that two agents don’t get the same goal. From the remaining goals, we chose the closest one to the second agent and remove it from the list. We continue in this fashion until all the agents have goals, or no potential goals exist anymore.

IV. Simulation

The simulation is done in a 30 m x 30 m x 3 m environment that contains 90 cylinder obstacles of radius 0.35 m and height 3 m. Their positions are generated randomly, following a uniform distribution. The environment is generated in Airsim [20]. The Gurobi solver is set to use one thread only as this resulted in faster computation
times during our simulations. All testing is done on the
Intel Core i7-9750H up to 4.50 GHz CPU and NVIDIA’s
GeForce RTX 2060 up to 1.62 GHz. We simulate up to 4
agents due to the limited computing power to run the Airsim
simulation, mapping/planning/control for each agent and the
global module. The agents communicate between themselves
using a ROS [26] topic. They also communicate with the
global module using a ROS topic.

A. Mapping parameters

The local map of each agent is of size $20 \times 30 \times 30 \times 3$ m.
The global map size is $30 \times 30 \times 30 \times 3$ m. The voxel size
used for both maps is 0.3 m. The update rate for the local
map is 10 Hz (lidar measurement frequency) and the update
rate of the global map is 5 Hz. Every time the global map
is updated, a new set of goals is computed and sent to each
agent. The local map update takes less than 1 ms due to the
GPU accelerated method we use [17] and the global map
update and goal computation takes less than 3 ms.

B. Planner parameters

We choose the following parameters: $N = 12$, $h =
100$ ms, $a_{\text{amp}} = a_{x, \text{max}} = a_{y, \text{max}} = a_{z, \text{max}} =
0.7 \cdot g$, $a_{z, \text{min}} = -g$, $j_{x, \text{max}} = j_{y, \text{max}} = j_{z, \text{max}} =
8 m/s^2$, $v_{\text{amp}} = 3.5 m/s$, $D_{\text{lim, max}} = \text{diag}(1,1,1)$,
$\text{thresh dist} = 0.4 m$, $P_{\text{hor}} = 2$. The weight matri-
ces are diagonal: $R_x = \text{diag}(200,200,200,0,0,0,0,0)$,
$R_{N} = \text{diag}(100,100,100,0,0,0,0,0)$ and $R_u =
\text{diag}(0.01,0.01,0.01)$. The drone radius is $d_{\text{rad}} = 0.3$ m.
The DMP planner pushes the JPS path 0.6 m (2 voxels) away
from obstacles (when possible). The planning frequency is
10 Hz. The planning requires synchronized clocks between
the agents. This is satisfied as all the agents use the same
CPU clock during the simulation. In a real world situation,
the clocks can be synchronized at the beginning of the
exploration since the drift is minimal (1 microsecond every
second) for the duration of an exploration task.

C. Controller parameters

The frequency of the MPC controller is 20 Hz. The
weights of the controller are:

\[
P = Q_x = \text{diag}(15,15,15,0.01,0.01,0.01,0,0,0,0.1) \quad (20)
\]

\[
R_u = \text{diag}(0.05,0.1,0.1,0.1) \quad (21)
\]

All parameters are set by approximation/experimentation and
may not be optimal. We limit $|\phi| \leq 85 \text{ deg}$, $\theta \leq 85 \text{ deg}$,
$|\dot{\phi}_{\text{cmd}}| \leq 120 \text{ deg/s, } |\dot{\theta}_{\text{cmd}}| \leq 120 \text{ deg/s and } |\dot{\psi}_{\text{cmd}}| \leq 60 \text{ deg/s.}$

D. Simulation results

We show the results of doing a series of 5 explorations
on 5 randomly generated maps using 1,2,3 and 4 agents in
Tab. II Also we also show the performance of 1 agent and 4
agents on the same map (Fig. 6). The starting position of
the first agent is (0,0,0) m. When using multiple agents,
the starting position of agents are offset from each others
3 m in the $x$ direction (Fig. 6). All agents stop moving
when the exploration is done i.e. all voxels are discovered as
free or occupied, or there is no path found for the remaining
undiscovered voxels.

The average flight distance per agent decreases in a way
that is approximately inversely proportional to the number
of agents used. The average flight velocity slightly increases
since an agent has less chances of being torn between two
close goals as other agents explore goals that are close to
it. The average exploration time which corresponds to the
time required to explore the full volume also decreases in
an approximately inversely proportional way to the number
of agents used. The average computation time increases as
we use more agents due to the fact that there are more
constraints that are added to each agent’s MIQP/MPC that
 correspond to the separating hyperplanes with other agents.
Note that the computation time can be decreased by lowering
the number of discretization steps $N$. Since the maximum
computation time is 64 ms, this would leave $100 - 64 =
36 ms$ to communicate the trajectory to other agents using
a broadcasting network (in our case a ROS topic). This
means that we can modify $N$ to lower the computation
time enough to satisfy communication constraints. Finally
we show the safety ratio which corresponds to the ratio:
(minimum distance between any two agents at any time
during the exploration)/(minimum collision distance). The

\begin{table}
\centering
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline
Number of agents & Flight distance (m) & Flight velocity (m/s) & Exploration time (s) & Computation time (ms) & Safety ratio \\
\hline
1 & 239.7 / 263.3 / 20.5 & 1.74 / 3.4 / 0.7 & 139.92 / 158 / 15.6 & 9 / 45 / 3.7 & - \\
2 & 129.5 / 137.7 / 7.72 & 1.8 / 3.47 / 0.74 & 78.2 / 83.3 / 4.67 & 12 / 49.8 / 4.7 & 1.12 \\
3 & 81.2 / 110.91 / 13.4 & 1.9 / 3.62 / 0.81 & 49.6 / 60.2 / 6.36 & 13 / 61 / 5.2 & 1.03 \\
4 & 73 / 86.8 / 9.2 & 2.04 / 3.9 / 0.88 & 44.9 / 50 / 4.27 & 14.5 / 64 / 5.3 & 1.13 \\
\hline
\end{tabular}
\caption{Comparison between 1,2,3 and 4 agents using our framework on 5 randomly generated maps of size $30 m \times 30 m \times 3 m$ and with obstacle density 0.1 $obst/m^2$. We show the mean / max / standard deviation per agent of each metric, except for the Safety ratio.}
\end{table}
planner satisfies safety constraints when using any number of agents.

V. CONCLUSIONS AND FUTURE WORKS

In this paper, we presented a novel framework for multi-agent autonomous collaborative exploration of unknown environments. The method uses recent advances in Safe Corridor generation, high-speed mapping and multi-agent planning to guarantee safety and computational efficiency during the exploration task. The framework is tested in a state-of-the-art simulator using up to 4 agents.

In the future, we plan to implement the exploration framework in a fully autonomous setting. This requires to add one more submodule in the local module for localization/odometry and account for localization uncertainty in the planning submodule to guarantee safety.

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