Research on Predicting the Bending Strength of Ceramic Matrix Composites with Process of Incomplete Data

Gao Xiang, Li Guanghui, Tan Rong, and Yao Leijiang

Abstract—With the rapid development of machine learning, it is possible to use neural networks to build models to predict performance of Ceramic Matrix Composites (CMCs) with raw materials and environments. In the traditional material science engineering, it always took a long time to develop a new CMC. Furthermore, there is still no theoretical basis providing references to design experiments to develop CMCs with ideal performances. This work proposed a model to predict the bending strength of CMCs with a Convolution Neural Network (CNN) using 8 factors considered to affect the bending strength of CMCs mainly. For the data were all collected from papers published on journals and conferences, and there is no standard to describe an experiment, the incompleteness of data influences the performance of our model seriously. Then we tried several methods to fill the data, finally the regression imputation with a dual-hidden-layer neural network performed a significant improvement of the CNN bending strength prediction model.

Index Terms—Bending strength, Ceramic Matrix Composites (CMC), Convolution Neural Network (CNN), imputation.

I. INTRODUCTION

Ceramic matrix composites (CMCs) are a subgroup of composite materials, which consist of various fibers embedded in a ceramic matrix. They not only possess the exceptional properties of ceramic such as the resistance to high temperature, the high strength and rigidity, the low density and the resistance of corrosion, but also improve the disadvantages like poor toughness and reliability. CMCs have great potential and have been applied in the areas of aeronautics, astronautics, automotive industry, et al.

In the traditional material science engineering, how to develop a new CMC was always a challenge to scientists, the experience and intuition of whom played an important role in making decisions on choosing the raw materials and environments of experiments. It is because of the lack of theoretical basis, and the development of new CMCs progresses slowly all the time.

In June, 2011, the United States government published Advanced Manufacturing Partnership (AMP) [1], a crucial part of which is Materials Genome Initiative (MGI) [2]. MGI is composed of computational tools, experimental tools and the digital data. The digital data contains all kinds of data and information from posted experiments, which is used to provide the basis of design for high throughput experiments.

In recent years, plenty of machine learning models appeared, which performed much better than traditional models on function fitting. Inspired by this, we tried four common methods to fit the experiment data collected from documents published to predict the bending strength of CMCs, which are support vector machine (SVM) [3], eXtreme Gradient Boosting (XGBoost) [4], deep neural network (DNN) and convolution neural network (CNN) [5].

Owing to the variety of the quality of documents, the lack of experiment factors exists in many documents, which results in the difficulty to train and predict using existing common models. Hence it is requisite to process the missing data. In this work, we tried three different methods to process the incomplete data, which are mean imputation, K-Means clustering imputation and DNN-based regression imputation [6]-[8].

II. THE BENDING STRENGTH PREDICTION MODEL

A. Data Preprocessing

As the basis, the interface type, the reinforcement fiber type and the perform type are all text data, they could not be processed with mathematic models. So, they were encoded into One-Hot codes [9].

As for the other factors, which are the reinforcement fiber type, the porosity, the interface thickness and the density, and the bending strength that is to predict are all digital data. They were scaled between 0 and 1 aiming to improve the performance of prediction models [10].

B. Prediction Models

We introduced four methods to build the bending strength prediction models.

SVM is a classical supervised learning model and usually used on small dataset. When SVM is used to fit a function, it is generally called support vector regression (SVR) [11]. XGBoost is an optimized distributed gradient boosting library implementing machine learning algorithms under the Gradient Boosting framework.

DNN, which is also as known as the multilayer perceptron (MLP), is a kind of function approximation model inspired by the neuroscience [12]. And is the most classical neural
network model. A deep feedforward network consists of several layers, and each layer is composed of several units operating in parallel [13]. CNN is to replace the matrix multiplication of at least one layer in a DNN into the convolution operation. It is of sparse interaction, which reduces computation and improves the computation efficiency that could describe the complex interaction among multiple variables [14].

When comparing the four methods mentioned above, we used $R^2$ score to evaluate their performance. It is a scalar ranging from 0 to 1 [15], the name of which is the goodness of fit, also known as the coefficient of determination and denoted $R^2$. The more $R^2$ is closed to 1, the better the model fits the data. It is one of the most significant indexes in the regression fitting [16].

C. Comparison of Models

For all four models, 90 percent of dataset were set to the training dataset, the other 10 percent was as the test dataset. We also used 10-fold cross validation to prevent overfitting. SVR is a distance-based model, so it usually is influenced by missing data obviously. The target of SVR is to find a hyperplane which could make the distances between points and itself small enough. The sketch is as Fig. 1 shows.

We replaced all missing values with zero to enable the model to work. The gamma and the penalty parameter $C$ are two hyperparameters need to be tested by the grid search. The gamma and itself small enough. The sketch is as Fig. 1 shows.

![Fig. 1. Sketch of SVR model.](image1.png)

In this work, the XGBoost is to build trees as shows. XGBoost is an open-source software library aiming to provide a "Scalable, Portable and Distributed Gradient Boosting (GBM, GBRT, GBDT) Library". XGBoost could process missing data well with its sparsity-aware split finding algorithm. This algorithm treats the non-presence as a missing value and learns the best direction to handle missing values. XGBoost is to build a certain number of trees, the sum of which is the target value to predict. While $n$ presents the number of training samples, $y$ presents the true value and the $\hat{y}$ presents the value predicted in last iteration, $loss$ presents the loss function, $f(x)$ presents a tree, $\Omega$ presents the regularization function, the objective function of XGBoost at iteration $t$ is as equation (1) shows.

$$Obj^{t} = \sum_{i=1}^{n} loss(y_i, \hat{y}_i + f_t(x_i)) + \Omega(f_t)$$

In fact, we also tried other optimization algorithms such as Stochastic Gradient Descent (SGD) and Adagrad, and other activation functions such as sigmoid and tanh function. The comparison result showed that the Adam and ReLU performed best. For this order of magnitude of data, 500 epochs are enough to reach very stable and good metrics, so all results of neural networks below are gotten after 500 epochs.

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We built a DNN model with two hidden layers, the architecture of which is as Fig. 3 shows.

![Fig. 3. DNN-based bending strength prediction model architecture.](image3.png)

| Layer  | 40 | 60 | 80 | 100 | 120 | 140 | 160 | 180 |
|--------|----|----|----|-----|-----|-----|-----|-----|
| 1st Layer | 0.02 | 0.43 | 0.79 | 0.83 | 0.73 | 0.90 | 0.78 | 0.88 |
| 2nd Layer | 0.57 | 0.93 | 0.74 | 0.94 | 0.84 | 0.77 | 0.90 | 0.54 |
| 3rd Layer | 0.79 | 0.96 | 0.74 | 0.94 | 0.91 | 0.90 | 0.83 | 0.54 |
| 4th Layer | 0.86 | 0.83 | 0.83 | 0.86 | 0.83 | 0.61 | 0.90 | 0.93 |
| 5th Layer | 0.76 | 0.93 | 0.76 | 0.84 | 0.95 | 0.87 | 0.79 | 0.83 |
| 6th Layer | 0.90 | 0.73 | 0.76 | 0.84 | 0.95 | 0.87 | 0.79 | 0.83 |
| 7th Layer | 0.19 | 0.95 | 0.94 | 0.11 | 0.79 | 0.84 | 0.83 | 0.95 |
| 8th Layer | 0.77 | 0.93 | 0.96 | 0.94 | 0.95 | 0.87 | 0.88 | 0.96 |
| 9th Layer | 0.08 | 0.80 | 0.91 | 0.96 | 0.97 | 0.83 | 0.81 | 0.84 |
We tried different numbers of neurons of each layer from 40 to 180 by grid search to find the best pair that could get the highest $R^2$ score while overfitting phenomenon is not obvious, the result is as Table I shows.

As Table I shows, the best $R^2$ score of DNN is 0.97. There is not an evident trend with the numbers increasing.

Then we tried to build a CNN model, the architecture of which is as Fig. 4 shows.

The filter and the batch size of the convolution layer, and the number of neurons of the fully-connected layer are three hyperparameters need to be optimized by grid search. We searched the batch size from 1 to 9, the filter size from 20 to 180 and the number of neurons of the fully-connected layer are three from 20 to 180. The grid search result is as Fig. 5 shows.

Finally, we found that when the batch size was 4, the filter size was 120 and the number of neurons of fully-connected layer was 140, the $R^2$ score on the test dataset reached the highest 0.9899 after 500 epochs.

The convolution layer executes a 1-D convolution function, which could extract information from multiple pieces of data by the convolution function more efficiently than fully-connected layer of DNN. The result also proved that CNN could get $R^2$ scores better and faster than DNN with less neurons.

The $R^2$ scores of four models mentioned above is as Table II shows.

As Table II shows, SVM performed not well. XGBoost got the best $R^2$ score for its ability to treat missing data. DNN and CNN also got high scores, and CNN performed better.

III. PROCESS OF MISSING DATA

Then we turned to consider if the missing data could be processed so that the $R^2$ score could be improved further.

A. Missing Data Statistic

The factors influencing the bending strength of CMCs mainly consist of 8 parts, which are the basis, the reinforcement fiber type, the reinforcement fiber volume content, the perform type, the interface type, the interface thickness, the porosity and the density [20].

We collected 170 pieces of data, 22 of which are incomplete and the statistic is as Table III shows.

B. Data Imputation

Algorithm I: K-Means Clustering Imputation

Input: data, data to imputation
Input: $K$

// Extract complete and incomplete data
$\text{d} \leftarrow \text{Complete}(\text{data})$
$\text{d} \leftarrow \text{Incomplete}(\text{data})$
$\text{Clusters} \leftarrow \text{KMeans}(\text{d}, K)$
$\text{Centers} \leftarrow \text{Mean}(\text{Clusters})$

// Find the cluster each $\text{d}_i$, denoted $\text{d}_i^*$ belongs to
for $\text{d}_i \in \text{d}$ do
  $m_i \leftarrow \text{Distance}(\text{d}_i^*, \text{Clusters}[0])$
  $m_i \leftarrow 0$
  for $i = 1$ to $\text{Size(Clusters)} - 1$ do
    if $\text{Distance}(\text{d}_i^*, \text{Clusters}[i]) < m_i$ then
      $m_i = \text{Distance}(\text{d}_i^*, \text{Clusters}[i])$
      $m_i = i$
  end if
  end for

// Use the center of cluster $d_i^*$, belongs to fill $d_i^*$
$\text{Fill}(\text{d}_i^*, \text{Centers}[m_i])$
end for

We tried three imputation methods, which are mean imputation, K-Means clustering imputation and DNN-based regression imputation.

Mean imputation is to replace any missing value with the mean of that variable for all other cases, which performs well when the values distribute around their mean values.

K-Means clustering imputation is a kind of unsupervised clustering algorithms. It needs to be assigned the number of clusters, denoted $K$. It is to divide all objects into $K$ clusters, making every object be nearest to the center of the cluster it belongs to. K-Means imputation clusters all complete pieces of data firstly, then contrasts every incomplete piece of data with the centers of clusters by their distances. A piece of incomplete data would be filling with the center, which is generally the mean, of the cluster nearest to it. The algorithm

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TABLE II: $R^2$ Scores Comparison of Four Models

| Algorithm     | SVM   | XGBoost | DNN   | CNN   |
|---------------|-------|---------|-------|-------|
| $R^2$ Score   | 0.7795| 0.9962  | 0.9731| 0.9899|

TABLE III: The Statistic of Missing Data

| Reinforcement Fiber Volume Content | Porosity | Density |
|-----------------------------------|----------|---------|
| 11                                | 1        | 10      |
is shown in Alg. 1.

For the K of K-Means clustering imputation needs to specified manually, we tried 18 numbers from 5 to 22. After finishing the imputation, the $R^2$ scores of the test dataset are as Table IV shows.

| TABLE IV: $R^2$ SCORES OF AFTER K-MEANS CLUSTERING IMPUTATION |
|-----------------|-----------------|----------------|----------------|----------------|
| K               | SVM             | XGBoost        | DNN            | CNN            |
| 5               | 0.7207          | 0.9970         | 0.8536         | 0.9265         |
| 6               | 0.7207          | 0.9970         | 0.9199         | 0.9404         |
| 7               | 0.7207          | 0.9970         | 0.8925         | 0.9245         |
| 8               | 0.7207          | 0.9970         | 0.8909         | 0.8896         |
| 9               | 0.7207          | 0.9970         | 0.8002         | 0.8757         |
| 10              | 0.7207          | 0.9970         | 0.8383         | 0.8828         |
| 11              | 0.7206          | 0.9970         | 0.8595         | 0.9471         |
| 12              | 0.7207          | 0.9970         | 0.9408         | 0.8984         |
| 13              | 0.7207          | 0.9970         | 0.7914         | 0.9299         |
| 14              | 0.7206          | 0.9970         | 0.5263         | 0.8780         |
| 15              | 0.7207          | 0.9970         | 0.8914         | 0.8733         |
| 16              | 0.7207          | 0.9970         | 0.8304         | 0.8900         |
| 17              | 0.7207          | 0.9970         | 0.9414         | 0.9078         |
| 18              | 0.7207          | 0.9970         | 0.9775         | 0.8973         |
| 19              | 0.7207          | 0.9970         | 0.8034         | 0.9445         |
| 20              | 0.7207          | 0.9970         | 0.9698         | 0.9562         |
| 21              | 0.7207          | 0.9970         | 0.9197         | 0.9310         |
| 22              | 0.7203          | 0.9970         | 0.9298         | 0.9110         |

As Table IV shows, after K-Means clustering imputation, SVM and XGBoost perform stably, while DNN and CNN are influenced by K obviously. $R^2$ score of SVM is lower than that of zero imputation. XGBoost performed a little better. DNN and CNN performed worse.

Regression imputation is a common imputation method in the traditional statistics that fits known data with a specified function to predict missing data. The fitting function is normally a linear function of a polynomial function, which performs not well when the data is extremely complex. Therefore, we used the regression imputation with neural networks as fitting functions to fill the incomplete data.

We build a DNN model with two hidden layers as the fitting function, the architecture of which is as Fig. 6 shows.

We also conducted grid search to get the best numbers of hidden layers of this DNN-based regression imputation model. Numbers of two hidden layers were tried from 20 to 160 with step 10. The imputation algorithm is as Alg. 2 shows.

After imputation methods above, $R^2$ scores of four models is as Table V shows. Hyperparameters were all optimized by grid search, and their scores in Table V are all the best.

As Table V shows, XGBoost performs very well and stably, which proves it is an ideal model to predict the bending strength. After DNN-based imputation, all models got a better $R^2$ score, in which CNN got the best 0.9998.

| TABLE V: $R^2$ SCORES OF FOUR MODELS AFTER IMPUTATION |
|-----------------|-----------------|----------------|----------------|----------------|
| Method          | Zero Imputation (No Process) | Mean Imputation | K-Means Clustering Imputation | DNN-based Regression Imputation |
| SVM             | 0.7795           | 0.7811         | 0.7207         | 0.8064         |
| XGBoost         | 0.9962           | 0.9962         | 0.9970         | 0.9982         |
| DNN             | 0.9731           | 0.7889         | 0.9698         | 0.9913         |
| CNN             | 0.9899           | 0.9536         | 0.9562         | 0.9998         |

Fig. 6. DNN architecture to implement regression imputation.

Algorithm 2: DNN-based Regression Imputation

Input: data, data to imputation
// Extract complete and incomplete data
d ← Complete(d)
d ← Incomplete(d)
col ← IncompleteColumns(d)
for col in col
  do
    $x \leftarrow d$.dropColumn(col)
    $y \leftarrow d$.extractColumn(col)
xtrain, ytrain, xtest, ytest ← SplitTrainTest(x, y, 10% test)
  scorebest ← 0
  i_best ← 0
  j_best ← 0
  for i = 20 to 160 step 10
    dnn ← DNN(i, j)
    dnn.fit(xtrain, ytrain) (10-fold cross validation)
    if $R^2$Score(dnn.predict(xtest), ytest) > best score
      i_best ← i
      j_best ← j
      scorebest ← $R^2$Score(dnn.predict(xtest), ytest)
    end if
  end for
  end for
dnnbest ← DNN(i_best, j_best)
pred ← dnnbest.predict(d.dropColumn(col))
fillColumn(col, pred)
end for

Fig. 7. Workflow of predicting CMCs bending strength with incomplete data.
IV. SYSTEM STRUCTURE

The entire system workflow is as Fig. 7 shows. To make the system easy to use for material researchers, we deployed it as a web application, the structure of which is as Fig. 8 shows.

The separation of front-end and backend is implemented by this web application. The front-end is based on Angular framework, and the backend is constructed with Django framework and TensorFlow, which are easy to scale out.

![Angular](image)

Fig. 8. Web application structure.

V. CONCLUSION

In this work, we collected experiments data of CMCs from documents, and tried to build models to predict the bending strength of CMCs with SVM, XGBoost, DNN and CNN. After grid search of hyperparameters, we found XGBoost, DNN and CNN all performed well, and XGBoost got the best performance. Then we experimented three methods to process incomplete data to research how to improve the robustness of the prediction model. By comparison, we found the DNN-based regression imputation could improve the performance of the prediction models considerably. Finally, the CNN bending strength prediction model with DNN-based regression imputation got the best R² score 0.9998, and XGBoost with this imputation also got a high score 0.9982. This work provides a valuable design reference for researching new CMCs.

We did not research deeper neural networks to build prediction model on account of the small amount of data. Further, we did not research the similarity, specificity and 3-D physical structure of different CMCs, which were only distinguished by encoding. In our opinions, it is a direction worthy of further study and improvement to mine and analyze these hidden factors.

CONFLICT OF INTEREST

The authors declare no conflict of interest.

AUTHOR CONTRIBUTIONS

Gao Xiang and Li Guanghui conducted the research; Tan Rong and Yao Leijiang analyzed the data; Gao Xiang and Li Guanghui wrote the paper; all authors had approved the final version.

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