1. INTRODUCTION

Once viewed as relatively simple objects that formed in a single, “monolithic” collapse, early-type galaxies are now widely believed to have been assembled hierarchically through repeated mergers and accretions (e.g., White & Rees 1978; Searle & Zinn 1978; White & Frenk 1991; Kauffmann & Haehnelt 2000; Cole & et al. 2000; Springel et al. 2005; Bower et al. 2006). A property of most luminous (e.g., $M_∗ \lesssim -22.5$) early-type galaxies is that they appear to have formed the majority of their stars at high redshift ($z \gtrsim 1$, corresponding to ages of $τ \gtrsim 7–8$ Gyr) and on short timescales ($Δτ \lesssim 1$ Gyr) (e.g., Bower et al. 1992; Franx 1993; Thomas et al. 1999; Trager et al. 2000; Wake et al. 2006). These features may be related to feedback from active galactic nuclei (AGNs), which can generate jets and outflows that blow away gas and suppress star formation (e.g., Silk & Rees 1998; King 2003; Murray et al. 2005; Fabian et al. 2006; Robertson et al. 2006). The general trends in the star formation histories of low- and intermediate-luminosity early-type galaxies are not as well understood, but they are known to show considerable diversity and to depend sensitively on environment (see, e.g., Tolstoy et al. 2009).

The discovery of the $M_{BH}–σ$ relation (Ferrarese & Merritt 2000; Gebhardt et al. 2000) points to a fundamental connection between the central black holes powering these AGNs and the dynamical properties of their host galaxies. There are several other galaxy properties that have also been found to scale with black hole mass, including luminosity (e.g., Kormendy & Richstone 1995; Ferrarese & Merritt 2000), light concentration (e.g., Graham et al. 2001), global velocity dispersion (e.g., Graham et al. 2001), global velocity dispersion (e.g., Graham et al. 2001), total gravitational mass of the host (Bandara et al. 2009). Thus, it has become clear that an understanding of the central regions of galaxies, including black holes and AGNs, is essential if we are to make sense of the formation and evolution of galaxies themselves.

However, the direct detection of black holes remains very challenging: see, e.g., Chapter 11 of Ferrarese & Ford (2005) for an overview of the observational difficulties. For kinematic measurements, a high central surface brightness is needed to obtain spectra of adequate signal-to-noise ratio (S/N), and this requirement can pose problems for massive early-type galaxies with shallow surface brightness profiles in their cores. At the distances of the Virgo and Fornax clusters, the small angular...
size of the black hole “sphere of influence” in most galaxies introduces a further complication. For example, at 20 Mpc, the distance of Fornax, a black hole in a galaxy with \( \sigma = 200 \text{ km s}^{-1} \) has a sphere of influence of only \( 0 \times 2 \) in radius (assuming the \( M-\sigma \) relation from Ferrarese et al. 2006b). It is therefore not surprising that a dynamical black hole mass measurement exists for only a single early-type galaxy in the Fornax cluster (FCC 213; Houghton et al. 2006; Gebhardt et al. 2007).

On the other hand, the correlation between a galaxy’s mass and that of its black hole was recently shown to extend down to the central nuclear star clusters found in low-mass galaxies (Ferrarese et al. 2006a; Wehner & Harris 2006). Other studies have reported similar relationships between black hole or nucleus mass and the host bulge luminosity, mass, and Sersic index (Rossa et al. 2006; Balcells et al. 2007; Graham & Driver 2007). These results are suggestive of a global relationship between galaxies and both types of central massive objects (CMOs; Côté et al. 2006); however, it is still an open question as to whether black holes and nuclei form via the same mechanisms or whether nuclei form first and serve as seeds for black hole formation.

The hydrodynamical simulations of Li et al. (2007) of a shared formation mechanism for both nuclei and black holes via the gravitational collapse of gas in bulgeless disks were able to reproduce a CMO and host mass correlation even without imposing an a priori \( M-\sigma \) relation, and were observed to be in agreement with Ferrarese et al. (2006a). Alternatively, Ferrarese et al. (2006a) noted that nuclei could, in principle, form in all galaxies, but that in massive galaxies, they might either collapse or be destroyed (or otherwise altered) by binary black holes. Using semi-analytic models, it was demonstrated by Devecchi & Volonteri (2009) and Devecchi et al. (2010) that nuclei could form at high redshifts and act as possible black hole seeds.

If nuclei and black holes form simultaneously, then it is possible that momentum feedback determines which object will eventually dominate the CMO mass. McLaughlin et al. (2006) noted that the same momentum flux that drives out gas from black holes (King 2003, 2005) could also regulate the growth of nuclear star clusters. Nayakshin et al. (2009) used this finding to explain why nuclei, not black holes, appear more likely to form in less massive hosts. Both objects can form simultaneously as gas is driven to the center of a galaxy through an event such as a merger, but it is the mass of the host bulge that sets the individual formation rates. Some evidence for such a scenario comes from observations of intermediate-luminosity galaxies (Filippenko & Ho 2003; González Delgado et al. 2008; Seth et al. 2008; Graham & Spitler 2009), as well as a number of dwarfs (Barth et al. 2004; Reines et al. 2011), that have been found to contain both a central stellar nucleus and a black hole. Indeed, using observations in the Virgo cluster, Gallo et al. (2010) estimated that nuclei hosting black holes could occur in 0.3%–7% of galaxies with stellar masses below \( 10^{11} \text{M}_\odot \), and in less than 32% of hosts above this stellar mass. In short, the study of nuclei presents us with a new opportunity to deepen our understanding of how galaxies and black holes co-evolve.

Like black holes, nuclei pose some observational challenges of their own. Although their existence in some dwarf galaxies has been known for decades, comprehensive surveys of galaxy clusters—in which the frequency of nucleation within complete galaxy samples could be robustly measured—did not appear until Binggeli et al. (1987) published their Virgo Cluster Catalog (VCC). This program observed 1277 members and 574 probable members of the Virgo cluster using the 2.5 m Las Campanas telescope; about 26% of all dwarf galaxies in the VCC sample were found to be nucleated. Shortly thereafter, a similar survey of the Fornax cluster by Ferguson (1989)—the Fornax Cluster Catalog (FCC)—found nuclei in 103/249 \( \approx 41\% \) of their dwarf galaxies. In the above studies, dwarf galaxies were identified primarily morphologically by their flat surface brightness profiles, although in general they were found to be fainter than \( M_B \approx -18 \text{ mag} \) (Sandage & Binggeli 1984).

Given the low luminosities and small sizes of most of these nuclei, the frequencies of nucleation estimated from ground-based photographic studies are certainly lower limits. For instance, Lotz et al. (2004) used WFPC2 on the Hubble Space Telescope (HST) to observe 69 dwarf elliptical galaxies in both Virgo and Fornax, finding nuclei in six galaxies that were previously classified as non-nucleated in the VCC and FCC. Based on wide-field imaging of Virgo dwarfs from the Isaac Newton Telescope, Grant et al. (2005) were able to identify many faint nuclei that were missed in the earlier photographic survey. In fact, the imaging of late-type galaxies with HST commonly revealed “nuclear clusters” that had gone unnoticed in earlier studies, with an overall frequency of nucleation of \( \approx 70\% \) (e.g., Carollo et al. 1998; Matthews et al. 1999; Böker et al. 2004; Walcher et al. 2005; Seth et al. 2006).

The first study to find a comparable frequency of nucleation among early-type galaxies was carried out by Côté et al. (2006, hereafter C06) with the Advanced Camera for Surveys (ACS) on HST, i.e., the ACS Virgo Cluster Survey (ACSVCS; Côté et al. 2004). In addition to establishing a high frequency of nucleation for early-type galaxies (at least 66% for galaxies brighter than \( M_B \approx -15 \)), the high-resolution imaging made it possible to characterize the detailed properties of the nuclei for the first time, including their luminosity function, structural properties, color–magnitude relation, and nucleus-to-galaxy luminosity ratio. We note here that although in C06 and this work we call the central excess of light rising above a galaxy’s extrapolated outer surface brightness profile a “nucleus,” these objects are not limited to being nuclear star clusters; certainly, some could be described as disks, bars, or other large-scale structures, which have been observed by previous studies of early-type galaxy centers (e.g., Ferrarese et al. 2006b; Balcells et al. 2007; Morelli et al. 2010). In this paper, which is part of the ACS Fornax Cluster Survey (ACSFCS), we examine the properties of nuclei belonging to galaxies in the Fornax Cluster, which is located at a distance of \( D = 20 \pm 0.3 \pm 1.4 \text{ Mpc} \) (statistical + systematic error; Blakeslee et al. 2009). This cluster is smaller, denser, more dynamically evolved, and more regular in shape than the Virgo cluster, and therefore allows us to study the properties of the nuclei of galaxies residing in a new and different environment.

Other papers in the ACSFCS series have described the data reduction procedures used in the survey (Jordán et al. 2007a, hereafter Paper I), systematic variations in the central structure of galaxies (Côté et al. 2007, hereafter Paper II), the logarithmic slope of the galaxies central surface brightness profiles (Glass et al. 2011, hereafter Paper IV), and the use of surface brightness fluctuations (SBFs) as a distance indicator (Blakeslee et al. 2009, hereafter Paper V). Paper III (2012, in preparation) of the ACSFCS will present a detailed isophotal analysis of the ACSFCS galaxies, including their dust properties, axial ratios, two-dimensional (2D) structure, total magnitudes, colors,
and surface brightness and color profiles. Papers studying the properties of globular clusters (GCs) in ACSFCS galaxies have examined their half-light radii (Masters et al. 2010, hereafter Paper VII), luminosity function (Villegas et al. 2010, hereafter Paper VIII), color–magnitude relation (Mieske et al. 2010, hereafter Paper IX), and color gradients (Liu et al. 2011, hereafter Paper X).

The outline of this paper is as follows. In Section 2, we describe the observations and methodologies used to measure photometric and structural parameters for the nuclei; in Section 3, we examine the nucleus properties, including their frequency of nucleation, luminosity function, sizes, surface brightness parameters, and colors; in Section 4, we put our results into the context of current formation scenarios; and in Section 5, we summarize our main results. The Appendix presents a comparison of one-dimensional (1D) and 2D methods for measuring photometric and structural parameters of nuclei and their host galaxies.

2. OBSERVATIONS AND ANALYSIS

The ACSFCS sample was constructed by selecting all galaxies from the FCC with (1) blue magnitudes \( B_T \leq 15.5 \) and (2) early-type morphologies, i.e., E, S0, SB0, dE, dE,N, or dS0,N. These morphological types were taken directly from Ferguson (1989), which are, in turn, based on the classification scheme of Sandage & Binggeli (1984). In addition to the 42 FCC galaxies that met these criteria, two ellipticals that lie just beyond the FCC survey region (NGC 1340 and IC 2006) were added, giving a total of 44 targets. Unfortunately, due to a shutter failure during execution, no images were obtained for FCC 161 (NGC 1379). Our final sample therefore consists of 43 early-type galaxies, which is complete (apart from FCC 161) down to a limiting magnitude of \( B_T \approx 15.5 \) mag (\( M_B \approx -16.0 \) mag). For all galaxies in this survey, membership in the cluster has been confirmed through radial velocity measurements. More details on the sample can be found in Papers I and III.

In Section 4.1, we will compare our results to a sample of galaxies and nuclei from the ACSVCS, which consists of 100 early-type members of the Virgo Cluster. That survey was magnitude-limited down to \( B_T \approx 12 \) mag (\( M_B \approx -19 \) mag) and 44\% complete down to its limiting magnitude of \( B_T \approx 16 \) mag (\( M_B \approx -15 \) mag). Both the Fornax and Virgo galaxies were observed with the ACS using Wide Field Channel (WFC) mode with the F475W and F850LP filters, which correspond closely to the \( g \)- and \( z \)-band filters in the Sloan Digital Sky Survey system (see, e.g., Fukugita et al. 1996; York et al. 2000; Sirianni et al. 2005).

Basic data for the ACSFCS galaxies are presented in Table 1. The ACSFCS identification number, the FCC number from Ferguson (1989), and any alternate names are reported in the first three columns. The table is ordered by increasing FCC blue magnitude, \( B_T \), which is given in Column 4. In calculating absolute magnitudes, we used the individual SBF distances measured in Paper V. Beginning in Section 3, all reported magnitudes are extinction-corrected, using dust maps from Schlegel et al. (1998), with the ratios of total-to-selective absorption in the WFC filters taken from Sirianni et al. (2005); the adopted \( B \)-band extinctions are shown in Column 5. The galaxy \( g \)- and \( z \)-band surface brightnesses at a geometric mean radius of 1″, measured by spline interpolation, are recorded in Columns 6 and 7. Note that all HST/ACS magnitudes quoted in this paper are AB magnitudes.

### Notes
- Column keys: (1) ACSFCS Identification number. (2) Galaxy name, mainly from the Fornax Cluster Catalog (FCC) of Ferguson (1989).
- (3) Alternative names in the NGC, ESO, or IC catalogs. (4) Total blue magnitude from ACSFCS (Paper III).
- (5) \( A_B \) from Schlegel et al. (1998). (6) and (7) The \( g \)- and \( z \)-band surface brightness measured at a geometric radius of 1″. (8) Nuclear classification in the FCC—Y: nucleated; N: non-nucleated; (9) Nuclear classification in ACSFCS—cS: core-Sersic (non-nucleated); S1: Sersic (non-nucleated); S2: double-Sersic (nucleated).

The final two columns in Table 1 give the classifications of the galaxies as nucleated from Ferguson (1989) and the ones derived from our surface brightness profile analysis. The parameterization of these profiles is discussed in Section 2.1, and the fitting methods used are outlined in Section 2.2. Finally, the nucleus properties obtained from the above procedure are described in Section 2.3. Additional information about...
our program galaxies, such as coordinates and morphological classifications, can be found in Papers I and III.

2.1. Parameterization of the Surface Brightness Profiles

As stellar nuclei, which are the focus of this study, are found in the luminous central regions of their host galaxies, accurately modeling the underlying galaxy surface brightness is necessary to measure their photometric and structural parameters. Indeed, for the faintest nuclei, or for some nuclei embedded in high surface brightness galaxies with steeply rising brightness profiles, this can be important for even identifying a central nuclear component (see Appendix A of C06). Using the IRAF task ellipse, which is based on the algorithm of Jedrzejewski (1987), elliptical isophotes with logarithmically increasing semimajor axis length were fitted to the galaxies. In most cases, all ellipse parameters (center, ellipticity, and position angle) were allowed to vary. However, to achieve convergence, the galaxies with large amounts of central dust required the ellipse centers to be held fixed throughout the fit (FCC 335, FCC 119, FCC 90), as well as the position angles and ellipticities while fitting the innermost areas (FCC 119 and FCC 90), where the fixed parameter values were determined by ellipse fits to the outer regions ($R_e > 5''$). For more details on the fitting procedures, see Section 3.2 of Ferrarese et al. (2006b) and Paper III.

The results from the ellipse isophotal analysis were used to derive azimuthally averaged radial surface brightness profiles, which were then fitted using one of three different parameterizations for the global surface brightness profile. The first parameterization is the well-known Sersic profile (Sersic 1968), a three parameter model which has the form

$$I_S(R) = I_e \exp \left( -b_n \left( \frac{R}{R_e} \right)^{1/n} \right),$$

where $I_e$ is the intensity at the effective radius, $R_e$, and the Sersic index, $n$, characterizes the overall shape of the light profile. The constant $b_n$ is defined such that $\Gamma(2n) = 2\gamma(2n, b_n)$, where $\Gamma$ and $\gamma$ are the complete and incomplete gamma functions, respectively (Clottì 1991). For lower values of $n$, the Sersic profile is shallow in the inner regions and steep in the outer regions; $n = 1$ produces a pure exponential profile, which generally provides a reasonable fit to dwarf galaxies. Higher values of $n$ yield functions which are steep in the inner regions and extended at large radii, with a less pronounced radial dependence on slope; these profiles generally fit bright ellipticals quite well (i.e., $n = 4$ reduces to a classical de Vaucouleurs profile).

Historically, these two types of profiles have been used to separately parameterize dwarfs and giants. However, more complete studies of galaxies have found that $n$ actually varies steadily with galaxy luminosity (e.g., Graham & GuzmÁE n 2003; Gavazzi et al. 2005; Ferrarese et al. 2006b; Kormendy et al. 2009; Misgeld & Hilker 2011; D. E. McLaughlin et al. 2012, in preparation). In what follows, we will refer to these single-component parameterizations as S1 models. Although the Sersic profile describes the outer component (typically beyond a few percent of the effective radius) of galaxies remarkably well—a consequence of the wide range in concentration, spatial scale, and surface brightness that is possible by varying $n$, $R_e$, and $I_e$, respectively—there can be variations in the central structure that cannot be accounted for in this simple model (see, e.g., Figures 1 and 2 of Paper II). Specifically, the brightest ellipticals tend to show a luminosity deficit in their central regions; for these objects, the six-parameter “core-Sersic” model (Graham et al. 2003) provides a good description of their surface brightness profiles. The core-Sersic model, referred to hereafter as a cS profile, can be written as

$$I_{cS}(R) = I' \left[ I + \left( \frac{R_b}{R} \right)^{a/\gamma} \exp \left( -b_n \left( \frac{R^a + R_b^a}{R_b^a} \right)^{1/an} \right) \right],$$

where

$$I' = I_b 2^{\gamma/a} \exp[b_n(2^{1/a} R_b/R_f)^{1/n}].$$

This parameterization consists of the usual Sersic profile, with an effective radius $R_e$ and Sersic index $n$, outside of a “break” radius $R_b$ (where the intensity is $I_b$). At $R_b$, the outer profile transitions to an inner power-law component with slope $\gamma$, according to the “sharpness” parameter $\alpha$ (where smaller values translate to smoother transitions).

By contrast, most of the low- and intermediate-luminosity galaxies in our sample show evidence for a luminosity excess in their cores which is, by definition, the signature of a central nucleus (see Appendix A of C06). A central excess in the surface brightness profile can then be modeled by adding a second Sersic component. This double-Sersic profile (which we denote hereafter as an S2 profile) has the form

$$I_{cS2}(R) = I_{e,1} \exp \left( -b_{n,1} \left( \frac{R}{R_{e,1}} \right)^{1/n_1} - 1 \right) + I_{e,2} \exp \left( -b_{n,2} \left( \frac{R}{R_{e,2}} \right)^{1/n_2} - 1 \right),$$

where the enumerated subscripts indicate the Sersic parameters for the outer and inner components.

It should be noted that, in C06, double-Sersic profiles were not used to fit the nucleated galaxies. Instead, the central nuclei were represented by King profiles (Michie 1963; King 1966), while the outer component was represented by either a core-Sersic or Sersic profile. Our decision to use a double-Sersic parameterization in the ACSFCS analysis is motivated by two considerations. First, modeling the inner component with the Sersic profiles allows for a diversity of possible physical systems, due to the range of the Sersic parameter (see above). For $n \sim 1$, the profile is a pure exponential and is thus suitable for embedded disks, whereas $n \sim 2$ represents Galactic GCs quite accurately, and presumably, nuclear star clusters as well. This is supported by the findings of Graham & Spitler (2009), who measured Sersic indices of $n = 3.0$, $2.3$, and $1.6$ for the nuclear star clusters of the Milky Way, M32, and NGC 205, respectively; and by Seth et al. (2010) who observed a Sersic index of $n \sim 2$ for NGC 404. Second, the use of Sersic profile for both the inner and outer components allows straightforward and convenient comparisons of their respective structural properties.

The overall trends described here are illustrated in Figure 1, which shows the systematic variations in the core and global structure of early-type galaxies along the luminosity function (see also C06; Ferrarese et al. 2006a, 2006b; Paper II, Paper IV). The upper panels in this figure show $15'' \times 15''$ images centered on five representative galaxies from the ACSFCS, 10 The ACSVCS finding of “luminosity excesses” in Virgo cluster galaxies relative to the inward extrapolation of Sersic models fitted to the outer profiles was subsequently confirmed by Kormendy et al. (2009) who reanalyzed a subset of the ACSVCS sample.
arranged in order of decreasing luminosity. The middle rows show model fits to the $g$-band surface brightness profiles as described above, i.e., FCC 213 (cS), FCC 83 (S1), FCC 277 (S2), FCC 136 (S2), and FCC 303 (S2). Note the systematic decline in galaxy surface brightness from left to right, and the emergence of an increasingly prominent central nuclear component as galaxy luminosity decreases. At low and intermediate luminosities, these luminosity “excesses” (i.e., nuclei) relative to the underlying galaxy model correspond to a steady steepening of the three-dimensional luminosity density on small scales, as shown in the lower panel of Figure 1 (from Paper IV). Images and brightness profiles for the full sample of ACSFCS galaxies will be discussed below.

### 2.2. Fitting Procedure

As described in Paper I, the ACSFCS uses the 
\textit{Lanczos3} kernel for drizzling rather than the Gaussian kernel which was selected for the ACSVCS. Due to the slightly larger distance of the Fornax cluster—20.0 versus 16.5 Mpc (Mei et al. 2007, Paper V)—and the fact that some of the Virgo nuclei were only marginally resolved in the ACSVCS (C06, Ferrarese et al. 2006a, 2006b), the sharper point-spread function (PSF) possible with the 
\textit{Lanczos3} kernel was deemed to be more important for the ACSFCS galaxies than the Gaussian kernel’s ability to repair bad pixels.

New PSFs for the ACSFCS were constructed in an identical manner using more than a thousand stars from the GO-10048 and GO-10375 programs to obtain photometric calibrations of the Galactic GC 47 Tucanae (PI: J. Mack). Using multiple observations allowed PSFs to be extracted from data that were acquired no more than two months away from the ACSFCS observation times; this proved to be important since on 2004 December 20, the secondary mirror of the HST was moved by 4.6 μm.

After running KINGPHOT (Jordán et al. 2005) on the GC candidates identified in the ACSFCS images,\(^{11}\) it was found that, for a subset of galaxies (FCC 213, IC 2006, FCC 193, FCC 249, FCC 277, FCC 19, and FCC 202), the mean half-light radius for GC candidates was significantly larger in the $g$ band than in the $z$ band, i.e., by roughly 0.5 pixels in F475W, which is much larger than the $\lesssim$0.1 pixel differences found in the ACSVCS. Anderson & King (2006) showed that the WFC PSF exhibits unpredictable variations on orbital timescales, particularly in the bluer filters, with differences in flux values of up to $\sim$10% in the central regions. To correct the seven galaxies whose imaging suffered from this variability, stellar sources in the individual images were used to empirically adjust the 47 Tucanae PSFs. Full details on this procedure are given in Paper I.

The azimuthally averaged, 1D surface brightness profiles were fitted using a \(\chi^2\) minimization scheme to determine if a Sersic or core-Sersic model was most appropriate. If visual inspection of the images and/or surface brightness profiles revealed a nucleus, then an S2 parameterization was adopted. At each iteration of the fitting procedure, the models used were convolved with the PSF in two dimensions (assuming spherical symmetry), and both the models and PSF were oversampled by a factor of 10 with respect to the ACS pixel size (i.e., they were sampled every 0.005 arcsec).

\(^{11}\) KINGPHOT fits two-dimensional, PSF-convolved King models to candidate GCs in the ACS images.
All profile parameters, except for intensity, were first fitted to both bandpasses simultaneously. These preliminary values were then used as initial guesses for the independent $g$- and $z$-band fits for most of the galaxies, with the exception of those with high central surface brightness that appear to be nucleated. In these galaxies, the nuclei are often quite extended and difficult to differentiate from the underlying galaxy light; thus, only the intensity parameters were allowed to vary between the two bands. As many previous investigators have noted, it is possible to reliably measure the total magnitudes and effective radii of marginally resolved stellar systems (i.e., star clusters, nuclei) using $HST$ imaging, whereas the concentrations can usually be constrained with considerably lower precision (Kundu & Whitmore 1998; Larsen 1999; Carlson et al. 2001; Jordán et al. 2005). This is understandable given that the measurement of concentration (or Sersic index) for a stellar system requires the curvature of the profile to be measured on scales smaller than the PSF. Fortunately, the derived radii and magnitudes are quite insensitive to Sersic index, at least insofar as the adopted model is an accurate representation of the actual nuclear profile.

A conservative resolution limit of 0\'\'025 was estimated in C06 based on the half-light radii of King models fit to stars classified as unresolved by KINGPHOT, and from the size of the central non-thermal point source found in VCC 1316 (M87). C06 further showed that most of their detected nuclei were more extended than point sources, by fitting point source profiles in addition to King profiles and comparing the residuals. Four of the nucleated galaxies (FCC 301, FCC 249, FCC 255, FCC S95) in Table 2 have best-fit effective radii that are measured to be smaller than our resolution limit in one, or both, photometric bands; these nuclei are thus unresolved—or nearly so—in their $HST$ imaging.

After some experimentation, we have estimated the uncertainties on the fitted parameters for the nuclei (and their host galaxies) using a Monte Carlo approach in which the $g$- and $z$-band surface brightness profiles for each galaxy are independently simulated 200 times. We included an amount of noise at each data point in the profile assuming a Gaussian distribution of errors and using the uncertainty on the intensity at each point computed by ELLIPSE. An additional source of error for the profiles comes from the determination of the background level, which we have also included by assuming a 10% error in the adopted background for each galaxy (estimated roughly by the galaxy-to-galaxy scatter in the measured background levels; see Figure 5 of Paper I). The errors on the magnitudes, colors, and effective radii estimated from these Monte Carlo simulations are given in Table 1. We hasten to point out that these errors do not include possible sources of systematic errors, such as errors...
in the PSF, and that they are therefore best viewed in a relative sense, and as lower limits on the true errors.

Finally, as a check on the (1D) method, we also fitted surface brightness profiles to our galaxies using 2D techniques. The full results of this analysis are described in the Appendix. In brief, the structural parameters obtained from the two procedures are largely in agreement, but due to the increased difficulty of characterizing complex structures using 2D fitting, we proceed with results from the 1D method, which we consider most appropriate for this study.

2.3. Identification of the Nuclei

The classification of a galaxy as nucleated or non-nucleated was performed in the following way. The program galaxies were all fitted with pure Sersic profiles outside of a geometric mean radius of 0.5′ (∼50 pc). The geometric mean radius was derived from the fitted elliptical isophotes and is thus defined as $R = a(1 - \epsilon)^{1/2}$, where $a$ is the semimajor axis and $\epsilon$ is the ellipticity. If an inward extrapolation of this profile revealed an excess of light in the center, then the full profile was refitted by adding a second Sersic component, and the galaxy was thus considered nucleated and classified as S2. In general, the level of nucleation was slightly greater in the $g$ band, as the nuclei are often found to be somewhat bluer than their hosts (see Section 3.6).

One of our program galaxies, FCC 119, appears to have a distinct nucleus offset that is from its photocenter by ∼0.7′. Due to the presence of dust in the inner regions of the galaxy, the ellipse centers were held fixed to the photocenter throughout the fit; thus, the nucleus is not apparent in the 1D surface brightness profile (discussed below). We therefore use parameters derived from a KINGPHOT fit to this object and consider this galaxy to be nucleated for the remainder of our analysis.

Galaxy classifications as nucleated or non-nucleated in the FCC, and our revised classification, are presented in Columns 8 and 9 of Table 1. In Table 2, we record the parameters of the Sersic profile fit to the nucleus of all S2 galaxies, as well as the KINGPHOT fit to FCC 119. Specifically, we have measured the $g$- and $z$-band integrated nucleus magnitudes (Columns 3 and 4), integrated and 4 pixel radius aperture nucleus colors (Columns 5 and 6), and $g$- and $z$-band half-light radii (Columns 7 and 8). Error estimates for each of these parameters are also included in this table, derived using the Monte Carlo approach described in Section 2.2. We have also calculated, by integrating the Sersic profiles, the fraction of luminosity occurring outward of $R > 0.5′$ (Columns 7 and 8).

Although the nucleus half-light radii in a few galaxies were measured to be somewhat larger in the $g$ band than in the $z$ band (i.e., FCC 310, FCC 177, FCC 95), we note that these are not the same galaxies that suffered from the variable PSF discussed in Section 2.2; for the most part, these differences reflect the fact that size measurements are particularly challenging for underluminous or extended nuclei in galaxies with steeply rising surface brightness profiles. For the reasons discussed in Section 2.2, we do not report the best-fit Sersic indices in Table 2, although we note that the indices for all nuclei in our sample have $0.5 \lesssim n \lesssim 4$, with a median of $n = 2.0 \pm 0.7$.

F475W images for the central 10″ × 10″ region of the program galaxies, where a distinct nuclear component is often discernible, are shown in Figure 2. The FCC number of the galaxy is labeled in each of the panels, along with the type of profile fitted; S2 therefore indicates that the galaxy was considered to be nucleated (that is, fitted with a double-Sersic profile). Individual fits to the azimuthally averaged $g$-band surface brightness profiles are shown in Figure 3. These images illustrate the systematic trend noted in Paper II, in which the central regions of early-type galaxies transition from shallow “cores” in the brightest systems (Ferrarese et al. 1994, 2006b; Lauer et al. 1995; Faber et al. 1997; Rest et al. 2001; Ravindranath et al. 2001) to a two-component structure (nucleus+galaxy) as one moves down the luminosity function, i.e., toward fainter, and lower surface brightness, galaxies.

3. RESULTS

In the following section, we analyze the properties of the ACSFCS nuclei derived from the above parameterization. Specifically, we examine the frequency of nucleation (Section 3.1), offset of the nuclei from their hosts (Section 3.2), nucleus-to-galaxy luminosity ratio (Section 3.3), and nucleus luminosity function (Section 3.4). Additionally, we compare their structural properties and scaling relations (Section 3.5), as well as colors (Section 3.6), with those of their host galaxies and GCs.

3.1. Frequency of Nucleation

Only 12 out of our 43 program galaxies were classified as nucleated in the FCC, which sets the frequency of nucleation at $f_n \approx 28\%$. Column 8 of Table 1 shows the classification as nucleated or non-nucleated in the FCC. These can be compared to our classification in the ACSFCS, where the use of the double-Sersic (S2) model indicates that we consider the galaxy to be nucleated. We find all galaxies previously classified as nucleated in the FCC to be nucleated in our sample, as well as an additional 19 objects, for a total of 31/43 galaxies, or $f_n \approx 72\%$.

The cause of this sharp rise in frequency of nucleation can be attributed to both observational selection effects and the definition of a nucleus as a central luminosity excess relative to a fitted galaxy model in our analysis. In the top panel of Figure 4, the open histogram shows the luminosity of all of the program galaxies, while the hatched and solid histograms denote those found to be nucleated in the ACSFCS and the FCC, respectively. The bottom panel of Figure 4 plots $f_n$, as a function of luminosity for the two surveys. The ACSFCS uncovers many more nuclei in more luminous host galaxies, as the high resolution of the WFC allows us to resolve nuclei in their high surface brightness cores. This selection effect is explored further in Figure 5.

Galaxy surface brightness at a geometric mean radius of $R = 1′$ (∼97 pc) was calculated using linear spline interpolation, in the $g$ and $z$ bands. By measuring surface brightness at a constant radius (rather than at some function of the effective radius), the result is a model-independent measure of central surface brightness, at a distance large enough to avoid the contribution from a typical nucleus, if present. Figure 5 plots the integrated nucleus magnitude derived from the S2 fit against galaxy surface brightness measured at a distance of 1″. The filled circles and open squares show the measurements for galaxies classified as nucleated in the ACSFCS and FCC, respectively. Clearly, the nuclei that went undetected in the earlier (photographic) survey come in two forms: bright nuclei that are embedded at the centers of galaxies with intermediate luminosity (which also have steeply rising profiles, see Figure 3) and faint nuclei belonging to the lowest luminosity galaxies. Needless to say, it

12 We include NGC 1340 and IC 2006 in this calculation; although they do not appear in the catalog of Ferguson (1989), both have “E” classifications in NED (i.e., non-nucleated ellipticals).
is possible that we too may be missing some nuclei, so we take $f_n \approx 72\%$ as a lower limit on the true frequency of nucleation in the ACSFCS sample.

### 3.2. Offset Nuclei

The offset of each nucleus from its host galaxy photocenter was measured for 28 of our 31 nucleated galaxies. For FCC 335, FCC 119, and FCC 90, the elliptical isophote fitting was performed with the ellipse centers held fixed, as convergence could not be otherwise achieved due to dust in their central regions. Thus, the offsets for these nuclei could not be measured using the technique described below, although we did examine their offsets using our 2D (GALFIT) analysis, and they are also included in this section.

For the remaining 28 galaxies in question, an analysis slightly different to that used in C06 was performed. In C06, the galaxy photocenter was determined by taking the mean of the positions of all fitted isophotes satisfying $1'' \leq R \leq R_e$. However, because of the possibility that isophotes might drift from the center due to bright sources in the field of view (causing an artificial offset in the photocenter calculated using the above method), we have adopted a different procedure in this work, where the photocenter and its error were determined by running ellipse to fit a single isophote with a semimajor axis length of approximately $R_e/2$. As in C06, the position and error of the centroid of the nucleus were taken as the smallest fitted ellipse from the full ellipse run. We note that the geometrical parameter errors output by ellipse are calculated from the errors of the harmonic fit, with the first and second harmonics removed. The errors from the photocenter and centroid were then added in quadrature to obtain the total error on the offset. The results of this procedure are plotted as the black filled circles in Figure 6. We find that almost all of the galaxies in our sample have an offset of less than $0''.1$. The four that do have a larger offset (FCC 63, FCC 193, FCC 177, and FCC 277) have $\Delta R_n > 0''.1$ in only one of the two bands.

We generally observe the offsets from our 2D analysis to be larger than those determined using our 1D method. This is due to the fact that the 2D fitting procedure does not allow the ellipse parameters to vary with radius and returns the model that best fits
the average parameters of the entire galaxy, giving more weight to the outer regions in the determination of the photocenter. Thus, for our 2D analysis, we are not concerned with offsets larger than $\sim 0.5\arcsec$, and only three galaxies are found to have offsets larger than this—FCC 119 ($0.65\arcsec$), FCC 324 ($0.70\arcsec$), and FCC 288 ($0.62\arcsec$). FCC 119 is fairly irregular in structure, with a significant amount of dust in its core. FCC 324 and FCC 288 are both low surface brightness, highly flattened galaxies, with no obvious clusters near the photocenter that may have caused source confusion with what we consider to be the nucleus. We conclude that in our sample, at most 10% of the nuclei are offset at the level of $0.5\arcsec$ or more, consistent with the findings of C06 for the Virgo cluster.

To measure any trend between offset and galaxy luminosity, we perform a weighted least-squares fit to the data from Figure 6. Using the offsets from our 1D analysis, we obtain

$$\log \Delta R_g = (-0.057 \pm 0.070) B_T - (0.87 \pm 1.06)$$
$$\log \Delta R_z = (0.19 \pm 0.09) B_T - (4.9 \pm 1.3),$$

and from our 2D analysis,

$$\log \Delta R_{2D} = (0.21 \pm 0.18) B_T - (4.1 \pm 2.7).$$

The slopes of these relations do not indicate any significant trend between offset and galaxy luminosity. The errors on the fitted parameters are the standard errors.

Finally, some of the galaxies in our sample that we do not find to be nucleated may, in fact, be “dIrr/dE transition” objects, where a nucleus could be in the process of formation. In particular, FCC 152 and FCC 26 are irregular in shape and contain many star clusters and significant amounts of dust in their central regions. It is possible that one or more of these clusters could be nucleus progenitors that will migrate inward through dynamical friction (see Section 4.3.1).

3.3. The Nucleus-to-Galaxy Luminosity Ratio

Previous studies of early-type dwarfs (Lotz et al. 2004; Grant et al. 2005; Graham & Guzmán 2003), including C06, found

A prototype for this class is VCC 1512 in the Virgo cluster which contains a prominent central excess that is composed of blue, densely packed star clusters.
that nucleus brightness increases with host galaxy brightness. Similar relations are known to exist for the nuclear clusters in late-type galaxies (see, e.g., Carollo et al. 1998; Böker et al. 2004). A plot of nucleus versus host galaxy magnitude, the latter calculated by integrating the Sersic profile best fitting the main galaxy component over all radii, is shown at the top of Figure 7. Weighted best-fit linear relations of the form

\[ g_{\text{nuc}} = \alpha g_{\text{gal}} + \beta \]

\[ z_{\text{nuc}} = \alpha z_{\text{gal}} + \beta \]  

were fitted to the data, where \( g_{\text{nuc}} \) and \( z_{\text{nuc}} \) are nucleus magnitudes and \( g_{\text{gal}} \) and \( z_{\text{gal}} \) are the galaxy magnitudes. The best-fit parameters \((\alpha_1, \beta_1, \beta_2)\) are given in Table 3, where the quoted errors are the standard errors. Results are given for two cases, fixing the slope at \( \alpha_2 \equiv 1 \) and allowing it to vary freely (shown respectively as the solid and dashed lines in the upper panel of Figure 7).

Since the best-fit slope of the nucleus–galaxy luminosity relation is very nearly one, we consider the possibility of a constant nucleus-to-galaxy luminosity ratio, \( \eta = L_n/L_g \), where \( L_n \) and \( L_g \) are nucleus and galaxy luminosity, respectively. In the bottom of Figure 7, \( \eta \) is plotted as a function of host galaxy magnitude in the same band. The values of the weighted means and standard deviations are given in Table 3, while the weighted mean ratio and standard error on the mean from both bands is

\[ \langle \eta \rangle = 0.41\% \pm 0.04\% . \]  

This is 0.11\% ± 0.06\% larger than the value of \( \langle \eta \rangle = 0.30\% \pm 0.04\% \) found in C06 (a 1.9\( \sigma \) discrepancy). At first glance, this might suggest that, at a given luminosity, early-type galaxies in Fornax were slightly more efficient in assembling their nuclei than those in Virgo; however, the difference is due to the use of Sersic rather than King models in fitting the ACSFCS nuclei. As Sersic profiles with even moderate \( n \) have somewhat extended wings, they increase the inferred luminosity of the nuclei relative to the King models (whose defining characteristic is a tidal truncation radius). Re-fitting the Virgo data with \( S_2 \) profiles confirms this conclusion—in Section 4.1.2, where the new fits to Virgo are presented, we find agreement between \( \eta \) for both clusters.

Finally, due to the definition of \( \eta \), the best-fit relation from Equation (7) can be recast in terms of \( \log(\eta) \) and galaxy magnitude, where \( \alpha_\eta = -0.4(\alpha_1 - 1) \) and \( \beta_\eta = -0.4\beta_1 \). This relation is plotted as the dashed line in the bottom panels of Figure 7. Although we do not see any trend between \( \eta \) and galaxy luminosity, we note that in a study of galaxies containing both a nucleus and a black hole by Graham & Spitler (2009), it was found that the ratio of total CMO mass to spheroid mass tended to decrease in more massive galaxies.

### 3.4. Luminosity Function

One mechanism for the formation of galaxy nuclei is through multiple mergers of GCs that sink to the galaxy center by

![Figure 2. (Continued)](image-url)
Figure 3. Azimuthally averaged surface brightness profiles for the ACSFCS galaxies. As in Figure 2, galaxies are ordered by blue magnitude, with luminosity decreasing from left to right, and from top to bottom. The black points plot the measured g-band profiles. The red curves show the fitted models with the two separate components (nucleus and galaxy) indicated by the dashed curves; their sum is shown as the solid curve. The dotted vertical lines are drawn at a radius of $0.02 R_e$ in all cases. The top right label denotes the galaxy FCC number, and the three types of fitted models are denoted in the bottom left, by $S_1$ (Sersic), $cS$ (core-Sersic), or $S_2$ (double-Sersic). Note that FCC 167 contains a prominent central dust disk (Figure 2, Paper III), so the models were fitted outside $R = 5''$.

(A color version of this figure is available in the online journal.)

Table 4

| Sample | Band | $m_{nuc}^0$ (mag) | $\sigma_n$ (mag) | $m_{gc}^0$ (mag) | $\sigma_{gc}$ (mag) |
|--------|------|------------------|-----------------|-----------------|-------------------|
| ACSFCS | $g$  | $20.21 \pm 0.01$ | $1.06 \pm 0.01$ | $24.24 \pm 0.01$ | $0.71 \pm 0.01$  |
| ACSFCS | $z$  | $19.12 \pm 0.01$ | $1.33 \pm 0.01$ | $23.15 \pm 0.01$ | $0.71 \pm 0.01$  |

Given in Table 4, where the errors on the fitted parameters are the standard errors. We find the luminosity function of the nuclei to be both brighter and have a greater spread than that of the GCs. The difference in the means is $\Delta = 4.03$ mag in each band, that is, on average the nuclei are $\sim 40 \times$ brighter than a typical GC.

In reality, since we find the nucleus-to-galaxy luminosity ratio to be roughly constant, the nucleus luminosity function should reflect that of the host galaxies (albeit with more scatter), and is most likely parameterized by a Schechter function truncated on both ends—on the bright end because we find no bright galaxies that are nucleated and on the faint end because our sample is magnitude-limited. To illustrate this, we show in Figure 9 a Schechter function overlaid on the $B$-band galaxy luminosity distribution of the FCC and the ACSFCS. We then apply cutoffs at $B_T = 12.5$ and 16 mag (so that we are left with the magnitude range of the nucleated galaxies in our sample), and scale it down...
Figure 3. (Continued)
The Astrophysical Journal Supplement Series, 203:5 (33pp), 2012 November

Turner et al.

Figure 4. Top: luminosity distribution of the 43 ACSFCS program galaxies (open histogram). The overlaid hatched histogram shows the distribution of the 31 galaxies classified as nucleated in this study, while the solid histogram shows the distribution of the 12 nucleated galaxies according to the FCC. Bottom: the percentage of nucleated galaxies (\(f_n\)) in this study (open squares) and in the FCC (solid squares). The approximate luminosity regimes where galaxies show central surface brightness “deficits” and “excesses” (i.e., nuclei) are indicated (see Paper II, Paper IV).

by 91% (since we have 34 galaxies in this magnitude range, 31 of which are nucleated), and shift the Schechter function over by +6.0 mag (which corresponds to an \(\langle \eta \rangle \) of 0.41%) and −0.4 mag (to convert roughly from \(B\) to \(g\)).

Finally, we convolve it with a Gaussian with \(\sigma = 0.87\) mag, the unweighted standard deviation of \(\eta\), to take the scatter around \(\langle \eta \rangle \) into account. The resulting function plotted over the nucleus luminosities shows good agreement, apart from a few bright outliers; specifically, the nuclei from FCC 63, FCC 47, and FCC 148 have \(B_T \lesssim 17\). Each of these galaxies have a complex central structure that may be contributing to their brightness, either by causing accurate nucleus parameterization to be more difficult or due to the fact that, in these cases, the nucleus itself may be more complex.

3.5. Structural Properties and Scaling Relations

Nuclei at the distance of the Fornax cluster are almost never resolved in ground-based imaging, as 1\(''\) corresponds to \(\approx 100\) pc at a distance of 20 Mpc. However, with ACS resolution it is possible to measure sizes for nuclei as small as 0\(''0.25\) (see C06). In Figure 10, we present a comparison of the effective radii of the ACSFCS nuclei and GC candidates. On average, the nuclei are larger in size, and have a much greater spread, than the GCs, although the considerable overlap between the two distributions shows that the most compact nuclei are very nearly the same size as typical GCs (Paper VII). The two most prominent outliers are the nuclei of FCC 63 and FCC 47; both of these nuclei were also found to be the brightest in our sample (see Section 3.4). Regardless, Figure 10 clearly demonstrates that the nuclei have a size distribution that peaks at compact sizes and an extended tail populated by larger nuclei. The median sizes of the full sample are found to be 0\(''0.073\) (7.2 pc) and 0\(''0.071\) (7.0 pc) in the \(g\) and \(z\) bands, respectively.

Figure 5. Galaxy surface brightness in the \(g\) band (top) and the \(z\) band (bottom) measured at a mean radius of 1\(''\), plotted against the magnitude of the nucleus. The filled circles show the 31 galaxies found to be nucleated by this study, while the open squares show the 12 galaxies classified as nucleated in the FCC.

Figure 11 shows scaling relations for the nuclei from ACSFCS and ACSVCS. In the upper panel, we plot the effective mass surface density, \(\Sigma_e \equiv M_\ast / 2\pi R_e^2\), against total stellar mass, \(M_\ast\), calculated from the observed \((g - z)\) colors and the relations of Bell et al. (2003). The lower panel shows effective radius as a

\[14\] We use the unweighted standard deviation in this case, because we are looking to reproduce the observed rather than intrinsic scatter.
The Astrophysical Journal Supplement Series, 203:5 (33pp), 2012 November

Turner et al.

Figure 7. Top: nucleus magnitude plotted against host galaxy magnitude for the nucleated galaxies in the ACSFCS; results for the $g$ and $z$ bands are shown on the left and right, respectively. The lines show the best-fit relations, with the slope held fixed at unity (solid) and allowed to vary (dashed). Bottom: nucleus-to-galaxy luminosity ratio, $\eta$, against host galaxy magnitude for the $g$ band (left) and the $z$ band (right). The solid and dotted lines show the mean value of $\eta$ and its $\pm 1\sigma$ limit, while the dashed line shows the best-fit relation given by the dashed line in the upper panel, recast in terms of $\log(\eta)$ and host magnitude.

Figure 8. Luminosity function for the nuclei (closed black circles) in the $g$ (top) and $z$ bands (bottom). The distribution of the ACSFCS GC candidates (open blue triangles) as well as the luminosity function of their turnovers (open red squares) from Paper VIII plotted for comparison. Both luminosity functions are derived by fitting normalized Gaussians. For the GC turnovers, each turnover magnitude was weighted by the number of GCs in the galaxy.

(A color version of this figure is available in the online journal.)

function of stellar mass. In both panels, we also plot ACSFCS GCs, and the sample of early-type galaxies in Virgo, Fornax, and the Local Group from D. E. McLaughlin et al. (2012, in preparation). As found by Jordán et al. (2005), the GCs have a size of $R_e \approx 3$ pc that is nearly independent of mass, while the early-type galaxies show a smoothly varying $M_\star-R_e$ relation.

Figure 9. Top left: a Schechter function plotted over the $B$-band galaxy luminosity distribution for all early-type galaxies in the FCC (open circles) and the ACSFCS sample (filled circles). Top right: the previous Schechter function truncated at $B_T = 12.5$ and 16, and reduced by 91%, so that it represents the nucleated galaxies in our sample. Bottom left: the previous Schechter function shifted by $+6.0$ mag, corresponding to a constant ($\eta$) of $0.41\%$, and $-0.4$ mag to convert from $B$ to $g$. It should now roughly correspond to the nucleus luminosity distribution, although without taking into account the scatter. Bottom right: the luminosity distribution of the nuclei (solid line), the previous Schechter function (dashed line), and the same Schechter function convolved with a Gaussian of $\sigma = 0.87$ mag, the unweighted standard deviation of $\eta_g$ (dotted line).

Figure 10. Distribution of half-light radii of the 31 nuclei identified in this study (black filled circles), as well as the candidate ACSFCS GCs (blue open triangles), measured in the $g$ (top) and $z$ bands (bottom). The vertical dotted lines indicate the adopted resolution limit of $\sim 0\rlap{.}^\prime 025$.

(A color version of this figure is available in the online journal.)
a reflection of the fact that galaxies form a non-homologous family (D. E. McLaughlin et al. 2012, in preparation). This figure highlights several other interesting properties of the nuclei. First, there is an obvious similarity in the scaling relations of the Fornax and Virgo nuclei; we shall return to this point and its implications for nucleus formation models in Sections 4.1 and 4.3. The addition of the ACSFCS nuclei also reaffirms the trend noted by C06 that the nuclei, unlike GCs, obey a size–mass relation that merges with the GC sequence at low mass. For reference, the dashed line in the lower panel of Figure 11 shows the predicted scaling relation for nuclei that are assembled from repeated GC mergers, $R_e \propto M_\ast^{0.38}$ (Bekki et al. 2004). The corresponding $\Sigma_e$–$M_\ast$ relation is shown in the upper panel. Based on structural parameters alone, we conclude that the GC merger model is broadly consistent with the data (although the extremely red colors of the brightest nuclei pose a challenge to this model in its simplest form). The two solid lines in the lower panel show relations of the form $R_e \propto M_\ast^{0.5}$ and $R_e \propto M_\ast$, which will be discussed in Section 4.3.1.

3.6. Nucleus Colors

As in C06, we find a relationship between nucleus colors and magnitudes with the brighter nuclei having redder colors and residing in more luminous hosts. This is shown in Figure 12, where we plot the nucleus 4 pixel aperture colors against the $g$-band magnitudes. Significant scatter is seen for the brighter galaxies, which are labeled with their FCC number. This scatter was also seen in C06, although in Virgo galaxies bright nuclei appeared to be preferentially red, while in the case of Fornax, bright nuclei are seen to scatter to both red and blue colors. The increased scatter in the color of the bright nuclei may simply reflect the more complex formation and enrichment histories in their inner regions of brighter, more massive galaxies: mergers, gas inflow, star formation, and GC accretion would naturally lead to a greater degree of scatter in the general color–magnitude trend. However, we caution that firm conclusions are difficult to draw, since at least part of the scatter is likely the result of larger observational errors, given the difficulty of measuring accurate photometric parameters for nuclei residing in luminous, high surface brightness galaxies.

Figure 12 also shows the weighted line of best fit for nuclei in host galaxies fainter than $B_T = 13.5$: 

$$(g - z)_{\text{nuc}} = -(0.059 \pm 0.034) g_{\text{nuc}} + (2.1 \pm 0.7).$$

Such color–magnitude (or possibly metallicity–mass) relations are generally thought to be a sign of self-enrichment in low-mass stellar systems (e.g., Dopita & Smith 1986; Morgan & Lake 1989; Brown et al. 1991; Recchi & Danziger 2005; Strader & Smith 2008; Bailin & Harris 2009). It would not be surprising to observe the same self-enrichment in nuclei, given the location of the nuclei at the centers of their host galaxies, where compressive tidal forces would aid in the retention of chemically enriched gas.

The colors of the nuclei compared to the mean color of their host galaxy’s GCs (calculated using the GC sample from Paper VIII) are examined in the right-hand panel of Figure 13.
Figure 12. Color–magnitude diagram for the 31 nuclei identified in this study, with colors derived using 4 pixel apertures. Point size is scaled with magnitude as indicated. The dashed line is the weighted best fit for galaxies fainter than $B_T = 13.5$. Galaxies with $B_T \leq 13.5$ or with unusually red or blue nuclei are labeled. The mean and standard errors of the mean for each luminosity bin are indicated by the outlined squares. Right: histogram of the nucleus colors showing a possible bimodal, or skewed, distribution.

We find only a very weak trend that redder nuclei also have redder GCs, where a weighted least-squares fit gives (with standard errors)

$$\langle g-z \rangle_{\text{nuc}} = (0.64 \pm 0.84) \langle g-z \rangle_{\text{glob}} + (0.30 \pm 0.83) . \quad (11)$$

Since mean GC color has been found to correlate with that of the host galaxy (e.g., Larsen et al. 2001; Peng et al. 2006), we might expect to find a relation between the colors of nuclei and their GCs, given that we also find a correlation between nuclei and galaxy colors, plotted in the left-hand panel of Figure 13. The weighted best-fit line with standard errors is given by

$$\langle g-z \rangle_{\text{nuc}} = (1.84 \pm 0.39) \langle g-z \rangle_{\text{gal}} + (1.29 \pm 0.47), \quad (12)$$

which indicates that bluer nuclei tend to lie in bluer host galaxies and vice versa. The nuclei are also found to have a larger range in colors, and are in most cases bluer, than their host galaxies.

In Figure 14, we show galaxy and nucleus colors as a function of host galaxy luminosity. The colors of both the galaxies and the nuclei are found to become redder with increasing host luminosity:

$$\langle g-z \rangle_{\text{gal}} = -(0.072 \pm 0.010) B_T + (2.3 \pm 0.1),$$

$$\langle g-z \rangle_{\text{nuc}} = -(0.13 \pm 0.04) B_T + (2.8 \pm 0.5), \quad (13)$$

where the errors on the fitted parameters are the standard errors. We find the nucleus colors to vary more steeply with host luminosity than those of the galaxies, although the trend for the nuclei is quite weak for galaxies fainter than $B_T \sim 13$. Examining the offset between galaxy and nucleus colors reveals that those nuclei that are redder than their hosts lie predominantly in high-luminosity galaxies. The weighted least-squares relation and standard errors for the color difference are given by

$$\Delta \langle g-z \rangle = (0.56 \pm 0.033) B_T - (0.54 \pm 0.48). \quad (14)$$

On average, we find the nuclei to be bluer than their hosts by $\langle \Delta (g-z) \rangle = 0.28 \pm 0.04$ mag. If we exclude the nuclei...
in galaxies with $B_T < 13$ (the regime in which the nuclei are found to be redder than their hosts) we obtain a mean offset of $(\Delta(g - z)) = 0.32 \pm 0.03 \text{ mag}$, where the errors are the standard error of the mean.

4. DISCUSSION

4.1. The Role of Environment: Comparison to the ACSVCS

As described in Section 1, our Fornax survey was preceded by a similar study of 100 early-type galaxies in the Virgo cluster (ACSVCS; Côté et al. 2004) where an investigation into the properties of the nuclei in ACSVCS galaxies was carried out by C06. Our prime motivation for a study of galaxies in the Fornax cluster is to provide a first glimpse into the properties of nuclei in two rather different clusters, and an assessment of the role played by environment in nucleus formation and evolution. The interested reader is referred to Section 1 of Paper I, which compares some key properties of the two clusters. Briefly, Virgo is overall a much larger cluster, with a mass almost 10 times that of Fornax ($M_{200} \sim 4.2 \times 10^{14} M_\odot$ versus $(1-7) \times 10^{13}$; McLaughlin 1999; Tonry et al. 2000; Drinkwater et al. 2001), and a velocity dispersion twice as large ($\sigma_v \sim 760$ versus $374 \text{ km s}^{-1}$ Binggeli et al. 1987; Drinkwater et al. 2001). Compared to the Virgo Cluster, Fornax is poorer (Richness Class 0 versus 1; Abell et al. 1989; Girardi et al. 1995) and more compact ($R_{200} \sim 0.7$ versus 1.55 Mpc). Its intracluster medium (ICM) has both lower temperature (1.20 versus 2.58 keV) and metallicity (0.23 versus 0.34 solar) (Fukazawa et al. 1998), with the Fornax electron density at a given radius being about one-fourth that of Virgo (Nulsen & Bohringer 1995; Paolillo et al. 2002).

In this section, we will directly compare the results from both surveys. While C06 used King profiles for the nuclei in their paper, the ACSVCS results have since been updated with Sersic model fits to the nuclei, which allows a fair comparison between the two studies. Distances from Paper V were used to calculate the absolute magnitudes and physical sizes for both the Fornax and Virgo galaxies. We note that the two surveys have slightly different cutoff magnitudes ($B_T \simeq 16$ for Virgo and $\simeq 15.5$ for Fornax) and that the distance modulus of Fornax is $\sim 0.5$ mag larger than that of Virgo (Paper V). Therefore, the Virgo galaxies can reach absolute magnitudes roughly 1 mag fainter than those in Fornax.

4.1.1. Frequency of Nucleation

In Figure 15, we plot the frequency of nucleation of the Virgo and Fornax program galaxies as a function of their absolute blue magnitude. The Virgo galaxies appear in red, and the Fornax galaxies are shown in blue. In the upper panel, we overlay histograms for all galaxies (hatched) and nucleated galaxies (solid). This figure demonstrates how the Virgo galaxy magnitudes extend to $\sim 1$ mag below those of Fornax, as explained above. Our Virgo sample contains 100 galaxies, 67 of which are found to be nucleated, so we obtain a total frequency of nucleation, $f_n = 67\% \pm 8\%$. This is in excellent agreement with the value of $f_n = 72\% \pm 13\%$ found for our full Fornax sample.

The bottom panel shows the frequency of nucleation in each luminosity bin. Both clusters exhibit very similar distributions with $f_n = 0$ for the bright galaxies, while fainter than $M_B \sim -19.5$, $f_n$ continuously stays above $\sim 70\%$. Since our Virgo sample has 84 galaxies below $M_B = -19.5$ and our Fornax sample has 35, we find the total frequency of nucleation for galaxies fainter than $M_B = -19.5$ to be $80\% \pm 10\%$ for Virgo and $89\% \pm 16\%$ for Fornax.

Both C06 and this study have shown that this sharp increase in frequency of nucleation compared to previous ground-based studies (the VCC and FCC) is due mainly to surface brightness selection (see Figures 7 and 8 in C06 and Figure 5 in this work), which can be attributed to the improved resolution and depth offered by the ACS imaging. That is, the excellent angular resolution of HST has allowed us to uncover previously undetected nuclei in both very high surface brightness galaxies, where the nuclei are difficult to distinguish from the main body, and low luminosity galaxies, in which the nuclei may lie below the magnitude limit of the older photographic surveys.

4.1.2. Nucleus-to-Galaxy Luminosity Ratio

As in Section 3.3 and Figure 7, absolute nucleus magnitude has been plotted against absolute galaxy magnitude in the top panels of Figure 16. Relations of the form of Equation (7) have been fitted using weighted least squares to the Virgo and Fornax samples, both separately and combined, and the parameters and standard errors are recorded in Table 5, the results of which are in agreement to within the errors for both galaxy samples.

We also plot nucleus-to-galaxy luminosity ratio $\eta$ as a function of absolute galaxy magnitude in the bottom panels of Figure 7. The values for the mean and standard deviations of $\eta$ are given in Table 5. Taking the mean nucleus-to-galaxy luminosity ratio of both data sets combined, we obtain the following values for each band:

\[
\langle \eta_z \rangle = 0.37\% \pm 0.04\% \\
\langle \eta_B \rangle = 0.34\% \pm 0.04\%,
\]

15 See https://www.astros++/users/VCSFCS/Data_Products.html
which gives a mean value for both bands of
\[
\langle \eta \rangle = 0.36\% \pm 0.03\%.
\] (16)

The quoted errors refer to the standard error on the mean.

Finally, we note that, due to the definition of \( \eta \), the best-fit relation from Equation (7) can be recast in terms of \( \log(\eta) \) and galaxy magnitude, where \( \alpha_0 = -0.4(\alpha_1 - 1) \) and \( \beta_2 = -0.4\beta_1 \). This relation is plotted as the dashed line in the bottom panels of Figure 7, and we find that we do not see any significant trend between the nucleus-to-galaxy luminosity ratio and galaxy magnitude.

4.1.3. Nucleus Luminosities and Sizes

In Figure 17, histograms of nucleus luminosities for both our Virgo and Fornax samples are compared. The parameters of the weighted maximum-likelihood fit of a normalized Gaussian to each sample are given in Table 6, where the errors on the fitted parameters are the standard errors. Although we find differences between \( \bar{m}_n \) in the two surveys, their amounts are comparable to the errors estimated for the nucleus magnitudes.

We plot a histogram of nucleus sizes in Figure 18 for both our Virgo and Fornax samples. Although there is a large range in size (the very large Virgo nucleus belongs to VCC 1178), most nuclei appear to have radii <10 pc. The typical sizes are in good agreement, with median values of 5.7 pc in the \( g \) band for both clusters, and 7.2 pc and 7.0 pc in the \( z \) band for Virgo and Fornax, respectively.

4.1.4. Other Properties

In addition to the above properties, we find the Virgo and Fornax nuclei to be remarkably similar in a number of other ways. First, and most obviously, both the ACSFCS and ACSVCS galaxies exhibit a trend along the luminosity function in which their central surface brightness profiles gradually change from having a luminosity “deficit” to an “excess”: see, e.g., Figures 3 and 4 in C06, Figure 1 of Paper II, Figures 2 and 3 here, as well as a detailed discussion of this trend in Paper IV. Plotting surface brightness against magnitude, the nuclei are found to have different scaling relations than the GCs (see Figure 18 in C06 and Figure 11 here). Although C06 used integrated nucleus colors in their study, our use of aperture colors may be a more appropriate comparison to the King profiles used to determine the integrated nucleus magnitudes. Indeed, the best-fit line parameters outlining the color–magnitude relation for the nuclei with \( B_T \leq 13.5 \), given by Equation (13) in C06 and Equation (10) in this work, are in good agreement.

Table 5

| Sample | Band | \( \alpha_1 \) (mag) | \( \beta_1 \) (mag) | \( \beta_2 \) (mag) | \( \langle \log(\eta) \rangle \) (dex) | \( \sigma \) (dex) |
|--------|------|---------------------|---------------------|---------------------|--------------------------------------|------------------|
| ACSFCS | \( g \) | 0.90 ± 0.17 | 3.99 ± 2.85 | 5.78 ± 0.14 | −2.31 | 0.32 |
| ACSVCS | \( g \) | 0.81 ± 0.11 | 2.79 ± 1.96 | 6.12 ± 0.15 | −2.46 | 0.47 |
| Combined | \( g \) | 0.80 ± 0.09 | 2.68 ± 1.60 | 6.04 ± 0.11 | −2.43 | 0.44 |
| ACSFCS | \( z \) | 1.06 ± 0.16 | 7.38 ± 2.97 | 6.22 ± 0.16 | −2.49 | 0.35 |
| ACSVCS | \( z \) | 1.02 ± 0.11 | 6.51 ± 2.07 | 6.21 ± 0.15 | −2.46 | 0.53 |
| Combined | \( z \) | 1.02 ± 0.09 | 6.63 ± 1.69 | 6.21 ± 0.11 | −2.47 | 0.49 |

Figure 16. Same as Figure 7, but using absolute magnitudes and including 67 ACSVCS and 31 ACSFCS nuclei. Top: nucleus magnitude plotted against host galaxy magnitude, for the Virgo (red squares) and Fornax (blue circles) galaxies found to be nucleated, in the \( g \) (left) and \( z \) bands (right). The lines show the weighted best-fit relations, with the slope held fixed at unity (solid) and allowed to vary (dashed). The red and blue lines correspond to fits to the Virgo and Fornax panels of Figure 7, and we find that we do not see any significant trend between the nucleus-to-galaxy luminosity ratio and galaxy magnitude.

Figure 17. Same as Figure 8, but using absolute magnitudes and including 67 ACSVCS and 31 ACSFCS nuclei. The luminosity functions for both the Virgo (red squares) and Fornax (blue circles) nuclei are shown, in the \( g \) band (top) and the \( z \) band (bottom). Both data sets have been fitted with a normalized Gaussian. (A color version of this figure is available in the online journal.)

Table 6

| Sample | Band | \( \bar{m}_n \) (mag) | \( \sigma_n \) (mag) |
|--------|------|---------------------|------------------|
| ACSFCS | \( g \) | −11.54 ± 0.03 | 1.58 ± 0.02 |
| ACSVCS | \( g \) | −11.45 ± 0.02 | 1.87 ± 0.02 |
| ACSFCS | \( z \) | −12.67 ± 0.03 | 1.70 ± 0.02 |
| ACSVCS | \( z \) | −12.80 ± 0.02 | 2.16 ± 0.02 |

In good agreement, with median values of 5.7 pc in the \( g \) band for both clusters, and 7.2 pc and 7.0 pc in the \( z \) band for Virgo and Fornax, respectively.
Overall, we find a striking similarity between the nuclei of Virgo and Fornax, despite the clear environmental differences between the two clusters. This agreement suggests that the physical characteristics of individual galaxy clusters (such as ICM density), or the processes that depend on them (such as ram pressure stripping efficiency), do not play a dominant role in the formation and evolution of nuclei in early-type galaxies. Thus, it seems we can consider the nuclei examined here as being representative of those in early-type galaxies in general.

### 4.2. Extension to Low Luminosity: Comparison to the Local Group

Although the ACSVCS and ACSFCS provide a reliable measurement of the nucleation frequency for galaxies brighter than $M_B \lesssim -15$ mag, it is instructive to consider the frequency of nucleation in galaxies fainter than this magnitude limit. We can do so by examining the members of the Local Group, where the smallest observed dwarf galaxies reach magnitudes as faint as $M_V = -1.5$ mag and can have effective radii on the order of $\sim 30$ pc (see, e.g., Martin et al. 2008). As sample completeness is a concern for such faint, compact systems, we focus on the subset of early-type galaxies brighter than $M_B \approx -8$.

At present, there are 25 known early-type galaxies in the Local Group brighter than this limit (compiled from Mateo 1998; McConnachie et al. 2005; Brasseur et al. 2011). Of these, only two (NGC 205 and M32) are brighter than the ACSVCS limiting magnitude of $M_B = -15$ mag (Mateo 1998), both of which are known to be nucleated (e.g., Kent 1987; Lauer et al. 1998; Mateo 1998; Butler & Martínez-Delgado 2005; De Rijcke et al. 2006). Moving down the luminosity function, six other galaxies at most may contain either nuclei or kinematically/structurally distinct features near their core, listed in order of decreasing luminosity: NGC 147 (De Rijcke et al. 2006), Sagittarius (Mateo 1998; Layden & Sarajedini 2000; Monaco et al. 2005; Bellazzini et al. 2008), Fornax (Coleman et al. 2004, 2005; Coleman & de Jong 2008), Sextans (Kley na et al. 2004; Walker et al. 2006), Andromeda II (McConnachie & Irwin 2006), and Ursa Minor (Kley na et al. 2003; Palma et al. 2003).16

16 Although it is traditionally classified as non-nucleated, we include the Fornax dSph in this list since GC #4 is located $\sim 1/2$ a core radius from the galaxy photocenter (see Figure 1 of Coleman & de Jong 2008), and might thus be classified as a dwarf with an offset nucleus if moved to the distance of the Virgo or Fornax clusters.
4.3. Formation and Evolution Models

The origin of nuclei remains an open theoretical problem, with two main avenues of nucleus formation presently considered most viable. The first proposes that a galaxy’s star clusters will experience orbital decay due to dynamical friction and spiral inward, eventually coalescing at the center of the galaxy. The second formation mode focuses on gas accretion at the center of the galaxy, followed by star formation. Some similarities in the scaling relations of nuclei and black holes (see Section 1) have also given rise to models that consider the formation of both types objects in a shared context. In this section, we shall examine theoretical studies of nucleus formation in light of our new results, as well as models that explore the relationship between nuclei and black holes.

4.3.1. Dissipationless Infall of Star Clusters

Tremaine et al. (1975) first suggested that the nucleus of M31 was formed from GCs that spiraled inward to the galaxy center due to dynamical friction, and this mechanism continues to offer an attractive explanation for the assembly of nuclei in at least some galaxies. Of course, not all clusters that come close to the center of a galaxy will necessarily contribute to the formation, or growth, of a stellar nucleus; as Capuzzo-Dolcetta (1993) showed, dynamical friction and tidal stripping are competitive processes, where GCs are more readily destroyed by large nuclei, limiting nucleus growth.

Nevertheless, some fraction of GCs are expected to avoid tidal disruption and could contribute to either nucleus formation or the growth of pre-existing nuclei. Evidence in favor of this process was described in Capuzzo-Dolcetta & Tesseri (1999), who pointed out that the radial distribution of GCs in galaxies is less centrally concentrated than the halo stars (see also McLaughlin 1995, 1999; Côté et al. 2001, 2003; Peng et al. 2008). Such “missing” clusters could have contributed to nucleus formation. The Monte Carlo simulations based on this premise by Lotz et al. (2001) predicted that nucleus luminosities for dEs with $−17 < M_B < −12$ were consistent with observations for the brighter galaxies within this range, although they were overestimated for less luminous ones. The overprediction of nuclear luminosities in their low-mass systems resulted from their short dynamical times—meaning that nuclei are able to grow very efficiently—in spite of the fact that these galaxies have relatively few star clusters (see, e.g., Peng et al. 2008).

Numerical simulations by Oh & Lin (2000) and similar higher resolution N-body simulations by Capuzzo-Dolcetta & Miocchi (2008a, 2008b) were able to successfully reproduce the observed surface brightness profiles of known nucleated galaxies. A dependence on local tidal field was found in the Oh & Lin (2000) model, where disruptive tidal forces on the outskirts of galaxy clusters would alter GC orbits, increasing the dynamical friction timescales and decreasing nucleation forces. The Capuzzo-Dolcetta & Miocchi (2008a, 2008b) models suggest that, if linear scaling is assumed, then the observed nuclei could have formed from the infall of tens, to hundreds, of GCs (see also Sections 4.9 and 5.2.4 of C06). Both simulations found that nuclei may begin to coalesce away from the galaxy photocenter, although to quite different extents, i.e., up to $\sim 0.3$ kpc and settling within $\sim 1$ Gyr in Oh & Lin (2000) and $\sim 4$ pc away in Capuzzo-Dolcetta & Miocchi (2008a, 2008b).

Other simulations by Bekki et al. (2004) were used to determine that the scaling relations of nuclei formed through mergers of GCs would be notably different than those of the GCs. In Section 3.5, we discussed that the predicted scaling relation for nuclei in these simulations, $R_e \propto M^{0.38}_B$, was generally in good agreement with observations (see Figure 11). More recent work by Bekki (2010) focused on simulations of star cluster infall due to dynamical friction in disk galaxies. He found that the effectiveness of dynamical friction did not depend strongly on bulge mass, but increased with smaller disk mass, and with larger disk mass fraction, galaxy surface brightness, and star cluster mass. The ratio of nucleus mass to disk mass was found to decrease as a function of increasing disk mass, with a mass ratio of $\gtrsim 0.4\%$ for smaller disks and $\lesssim 0.1\%$ for disks with masses $M \gtrsim 10^9 M_\odot$. Additional models from Agarwal & Milosavljević 2011 were used to determine that the nucleus-to-host mass fractions of nuclei formed via young cluster accretion in both spheroids and disks (of stellar masses $10^9 M_\odot$ and $5 \times 10^9 M_\odot$ respectively) depended sensitively on the initial cluster mass function (ICMF). Using the nucleus mass fraction results of C06, Böker et al. (2004) and Walcher et al. (2005) to estimate the maximum ICMF mass found this result to be consistent with other observational and theoretical estimates.

However, star cluster mergers onto a disk may not be sufficient to explain nuclei formed in $M_V \sim −19.5$ spirals. N-body simulations by Hartmann et al. (2011), which aimed to reproduce the observed kinematics of the nuclei in M33 and NGC 4244, found that star cluster accretion onto a disk did not produce the necessary line-of-sight velocity increase, and at least half of the nucleus mass had to come from gas dissipation. Additionally, Antonini et al. 2012 performed N-body simulations of the Milky Way nuclear cluster, including the presence of a central SMBH, and found that the nuclear cluster luminosity function was consistent with 50% of the mass coming from GCs, and the other 50% due to continuous star formation.

Some provisional evidence for dissipationless formation in at least some galaxies was presented in Paudel et al. (2011), who used optical spectroscopy for Virgo cluster dwarfs to study both their stellar populations and their nuclei. Despite the small sample and the different environment (Virgo versus Fornax), their data present an interesting opportunity to speculate on the possible formation mechanisms for the ACSFCS nuclei. Paudel et al. (2011) found that nuclei in a handful (5) of the faint ($−16 < M_B < −14$) galaxies in their sample were older and more metal poor than their hosts, which is certainly suggestive of a connection to GCs. At higher luminosities, most of their nuclei were found to be younger than their hosts. While inconsistent with nucleus formation from old GCs, this observation may still be compatible with cluster infall, as our observations and many others have shown that ongoing star cluster formation can be present throughout some galaxies (e.g., Anders et al. 2004; Kyeong et al. 2010). In the ACSFCS sample, FCC 119, FCC 90, and FCC 26 are possible examples of $M_B > −19.5$ galaxies with young cluster systems.

Other suggestive observations come from Georgiev et al. 2009, where nuclei were identified serendipitously within a sample of GCs from nearby dwarf galaxies. The projected galactocentric distance used to classify these nuclei was determined using their luminosities and a required dynamical friction timescale of $\sim 5$ Gyr. Some of the nuclei were found to be offset by $\sim$tens of parsecs, which could be evidence for recent infall.

Additional support for such a scenario may come from the GC luminosity functions in Virgo and Fornax galaxies. The widths of GC luminosity functions are known to decrease
Note the sharp decline in $T$ where $b$ (see the lower panel of Figure 11), while the dotted red curve shows the end of the luminosity function may be caused, at least in part, by a slight decrease in turnover mass (Jordán et al. 2006, 2007b, Paper VIII). This truncation of the GC population on the bright side shows calculations for initial GC radii, $R_i$, equal to the galaxy effective radii (see the lower panel of Figure 11), while the dotted red curve shows $R_i$ fixed to 1.3 kpc, the median effective radius for ACSFCS galaxies. In both cases, $T_{DF}$ is plotted for five GC masses: 0.1, 0.25, 0.5, 1.0, and 2.0 million solar masses. Note the sharp decline in $T_{DF}$ for low-mass galaxies.

(A color version of this figure is available in the online journal.)

Figure 19: Top: histogram of masses for the 143 galaxies from the ACSVCS and ACSFCS surveys. Bottom: dynamical friction timescales, $T_{DF}$, plotted as a function of galaxy mass. Two sets of curves are shown. The dashed blue curves show calculations for initial GC radii, $R_i$, equal to the galaxy effective radii (see the lower panel of Figure 11), while the dotted red curve shows $R_i$ fixed to 1.3 kpc, the median effective radius for ACSFCS galaxies. In both cases, $T_{DF}$ is plotted for five GC masses: 0.1, 0.25, 0.5, 1.0, and 2.0 million solar masses. Note the sharp decline in $T_{DF}$ for low-mass galaxies. This truncation of the GC population on the bright side shows calculations for initial GC radii, $R_i$, equal to the galaxy effective radii (see the lower panel of Figure 11), while the dotted red curve shows $R_i$ fixed to 1.3 kpc, the median effective radius for ACSFCS galaxies. In both cases, $T_{DF}$ is plotted for five GC masses: 0.1, 0.25, 0.5, 1.0, and 2.0 million solar masses. Note the sharp decline in $T_{DF}$ for low-mass galaxies.

significantly with galaxy luminosity, a trend that is apparent by a slight decrease in turnover mass (Jordán et al. 2006, 2007b, Paper VIII). This truncation of the GC population on the bright end of the luminosity function may be caused, at least in part, by the shorter dynamical friction times as galaxies become less massive, although other (external) processes could also play a role (see Section 7.2 of Jordán et al. 2007b).

We revisit the question of star cluster infall efficiency by calculating the dynamical friction timescale, $T_{DF}$, for all galaxies in our ACS surveys of Fornax and Virgo. The upper panel of Figure 19 shows the distribution of galaxy masses from the combined surveys (filled histogram), while the lower panel shows the dependence of $T_{DF}$ on galaxy mass, $M_*$, which is given by

$$T_{DF} = \frac{2.64 \times 10^2}{\ln \Lambda} \left( \frac{R_i}{2 \text{ kpc}} \right)^2 \left( \frac{v_c}{250 \text{ km s}^{-1}} \right) \left( \frac{10^6 M_\odot}{M_{GC}} \right) \text{ Gyr.}$$

(17)

Here, $R_i$ is the initial galactocentric radius of the star cluster, $v_c$ is the circular velocity of the (assumed isothermal) galaxy, and $M_{GC}$ is the mass of the star cluster (Binney & Tremaine 2008). In this equation, $\ln \Lambda$ is the coulomb logarithm, which is defined as

$$\ln \Lambda = \ln \left[ \frac{b_{\text{max}} v_c^2}{G(M_{GC} + m)} \right],$$

(18)

where $b_{\text{max}}$ is the maximum impact parameter between the cluster and the interacting particle (a star of mass $m$). Following Lotz et al. (2001), we assume $v_c \approx \sqrt{2\sigma}$ where $\sigma$ is the integrated-light velocity dispersion measured within $R_e/4$ from D. E. McLaughlin et al. (2012, in preparation). We also take $b_{\text{max}} = R_e$ for all galaxies, with $R_e$ measured directly from the ACS imaging (see Section 3.5 and Figure 11).

Calculations have been carried out for five different star cluster masses (i.e., 0.1, 0.25, 0.5, 1, and 2 million solar masses) and for two assumptions for $R_i$. In the first case, we take $R_i = R_e$ (see also Lotz et al. 2001) which is shown as the dashed blue curves in Figure 19. In the second case, we simply fix $R_i$ at the median effective radius, 1.3 kpc, for all galaxies in the ACSFCS sample. The results in this case are indicated by the dotted red curves in Figure 19. Although $T_{DF}$ clearly varies with the assumed cluster mass and the precise choice of $R_i$, the strong mass dependence noted by previous investigators is clearly apparent in this figure. In particular, the dynamical friction timescales are dramatically shorter in galaxies with $M_\odot \lesssim 10^{10} M_\odot$ compared to higher-mass galaxies. We conclude that star cluster infall seems like a viable, indeed a likely, candidate for the growth of nuclei in low- and intermediate-mass galaxies in our sample. For the highest-mass galaxies, the mechanism appears much less viable given the fact that, in these systems, $T_{DF}$ greatly exceeds the Hubble time for all but the most massive and centrally concentrated star clusters.

Finally, we conclude this section with some final remarks on Figure 11, which compared the structural parameters of nuclei to those of GCs and their host galaxies. While there is, as noted in Section 3.5, good agreement with the nucleus size–mass relationship found by Bekki et al. (2004) from simulations of GC mergers, there are reasons to believe that a single relation cannot be appropriate for all nuclei which, in our sample, span more than four decades in mass. For comparison, the simulated nuclei of Bekki et al. (2004) span a factor of just 10 in mass. It is to be expected that the precise form of the size–mass relation in the context of the GC merger model will be different in different mass regimes. For instance, when only a small number of mergers contribute to the nucleus, we expect from the virial theorem and conservation of energy that $R_e \propto M_\odot^{1/5}$. At later times, when the mass of the nucleus greatly exceeds the mass of an accreted GC, the relation should steepen to $R_e \propto M_*$. These scaling relations, shown in the lower panel of Figure 11, are in good agreement with the observed sizes and masses.

All in all, based on the existing data, we believe that cluster infall must have played an important role in the formation of the nucleus of the low- and intermediate-mass hosts within our sample. At the same time, the red colors of some of the largest and most massive nuclei (Section 3.6) present a strong challenge to this model, suggesting that an additional process—most likely the dissipational infall of metal-rich gas—likely begins to dominate the formation of nuclei in galaxies of progressively larger masses (Mihos & Hernquist 1994; C06; Paper II; Hopkins et al. 2008, 2009).

4.3.2. Dissipational Infall of Gas

It has long been suspected that nuclei could form through star formation following the accretion of gas in galaxy centers (van den Bergh 1986), although the exact origin of the gas, and the mechanism that triggers the inflow, is matters of debate.

In some models, the gas is assumed to originate from outside the galaxy. Davies & Phillipps (1988) proposed that dEs may be formed from fading stellar populations in dwarf irregulars, where the accretion of H I gas induced starbursts, the final one

Recall that in the Milky Way, the GC mass corresponding to the peak of the luminosity function is $2.4 \times 10^5 M_\odot$ (McLaughlin 1999).
occurring in the center and forming the nucleus. Silk et al. (1987) predicted that the intergalactic medium (IGM) could fall into dwarf galaxies when it is cooled and compressed during group formation. This model noted that dwarfs closer to large galaxies may not be able to form nuclei as efficiently, since the large galaxy’s tidal field makes it difficult for the dwarf to capture the gas. Babul & Rees (1992) found an opposite trend with environment: they observe that nucleus evolution may depend on local IGM density, because this determines whether supernova-driven gas outflows are able to escape. Dwarfs in low-pressure regions would have their gas ejected and then fade away, while winds in dense environments would be restricted to the starburst region by the IGM. This confinement could cause gas to cool and recollapse, creating two short or one prolonged starburst.

Gas might also be funneled to the centers of galaxies which have disks and axisymmetric features. Milosavljević (2004) suggested that in spiral galaxies, magneto-rotational instability in the disk transports gas to the center. Bekki et al. (2006) and Bekki (2007) performed chemodynamic simulations of the inner 1 kpc of dwarf galaxies with stellar masses of \(2.5 \times 10^7 \leq M_{\text{gal}} \leq 1.0 \times 10^9\), to explore the remnant created through dissipative merging of stellar and gaseous clumps formed from nuclear gaseous spiral arms in a gas disk. The simulations produced nuclei that were rotating and flattened, consisting of stars with varying ages and metallicities. Although the initial clump was found to form off-center (about 200 pc by visual inspection of the simulation data), it would fall into the center within 100 Myr. They found that overall, the nuclei were characteristically younger and more metal rich than the host, with more massive hosts creating more metal-rich nuclei. Gas settling timescales increased with decreasing dwarf mass (due to feedback being more effective in smaller galaxies), so low-mass dwarfs were found to have younger and bluer nuclei. More massive and dense nuclei were formed in more massive dwarfs with deeper central potentials, and both the mass and mass fraction of the nucleus were found to increase with spheroid mass. Nuclei in high surface brightness galaxies should also have higher surface brightness, owing to the increased dynamical friction due to higher stellar densities. The nucleus surface brightness was strongly dependent on the gas fraction of the host, and thus may be more likely to form in this manner in late-type galaxies with relatively large amounts of gas. Finally, the addition of a central black hole to the simulation had little effect on the properties of the remnant nucleus.

Another source of nuclear material, which was first proposed by Bailey (1980), could arise from stellar winds. It was found that only a small (\(\sim 10^5 M_\odot\)) amount of gas was needed to cause an inflow for an elliptical galaxy with \(M_{\text{gal}} \sim 10^{11} M_\odot\). Seth (2010) observed that such a mechanism could produce the age, abundance gradient, and rotation curve seen in the nucleus of M32.

The dissipative inflow of gas to the galaxy center can also be induced by galaxy mergers. Mihos & Hernquist (1994) performed \(N\)-body simulations of disk galaxy mergers, where they found that gas dissipation and the star formation that followed created dense stellar cores in the remnant. Similar higher resolution simulations by Hopkins et al. (2008, 2009) showed that gravitational torques during gas-rich mergers removed the angular momentum of the gas, which would then undergo gravitational collapse. The amount of gas inflow was found to largely depend on the progenitor galaxy’s gas fraction, while the addition of a central black hole was not found to have a significant effect on the properties of the final remnant. Unfortunately, these models lacked the resolution to study typical nuclei, particularly those in the low-mass galaxies, i.e., apart from a small number of cE galaxies in the ACSVCS sample, which have likely been heavily tidally stripped (e.g., Faber 1973; Ferrarese et al. 2006b; Côté et al. 2008; Chilingarian et al. 2009; Huxor et al. 2011; D. E. McLaughlin et al. 2012, in preparation), the simulated galaxies of Hopkins et al. (2009) have masses \(\geq 10^{10} M_\odot\), more than 10 times larger than the masses of the faintest galaxies in the ACS surveys. However, in this restricted mass regime, the properties of these simulated galaxies are in good agreement with our ACSFCS (and ACSVCS) observations.

Likewise, the simulations of Bekki et al. (2006) and Bekki (2007), which instead focused on the low-mass galaxies, also appear to be consistent with observations, including those from our \textit{HST}/ACS imaging and results from ground-based spectroscopy. First, the nuclei in these simulations were found to be younger and more metal-rich than their hosts, with the metallicity of the nucleus increasing with host mass, a trend that was seen in Paudel et al. (2011). Second, their finding that low-mass dwarfs have younger and bluer nuclei is consistent with some of the nuclei from Paudel et al. (2011), and with the nucleus colors observed in our study. Finally, they also found that the mass fraction of the nucleus increased with host spheroid mass, and that their simulated surface brightness profiles showed nuclei which become more prominent with increasing dwarf mass, whereas in low-mass dwarfs the nuclei were barely distinguishable. It is therefore possible, as discussed in Section 4.3.1, that nucleus formation through gas infall may be most significant for intermediate- and high-mass galaxies. In their analysis of the ACSVCS, C06 (p. 87) noted that some of the reddest and brightest nuclei “may be candidates for the \textit{dense stellar cores} that form in numerical simulations (Mihos & Hernquist 1994) when (chemically enriched) gas is driven inward, perhaps as a result of mergers.” Such a result can be reconciled with our nearly constant nucleus-to-galaxy luminosity ratio if star cluster infall accounts mainly for nucleus build up in lower-mass galaxies. At intermediate masses, both processes could contribute significantly to the growth of nuclei; candidates for such hybrid nuclei in the ACSFCS include FCC 43, FCC 249, FCC 310, FCC 148, and FCC 301, which may consist of both compact and extended components.

This basic scenario is also consistent with the general view that mergers (which can drive gas to the central regions of a galaxy) become increasingly important as galaxy luminosity increases, a consequence of the hierarchical merging paradigm. The observation that galaxy concentration—parameterized by Sersic index \(n\)—varies smoothly with galaxy luminosity (e.g., Jerjen & Binggeli 1997; Graham et al. 2003; Ferrarese et al. 2006b; D. E. McLaughlin et al. 2012, in preparation; see also Section 2.1) provides strong supporting evidence for this picture, as violent relaxation of merger remnants is thought to be responsible for the creation of de Vaucouleurs profiles (e.g., Barnes 1988, 1992), while the Sersic index of both bulge and disks of spirals has been shown to increase after satellite infall (Eliche-Moral et al. 2005). Figure 20 shows the dependence of two fundamental parameters for nuclei—luminosity fraction and effective radius—against the host galaxy Sersic index (Paper III). Those galaxies whose internal structure has likely been transformed most extensively through mergers, accretions, and harassment (i.e., those galaxies with high Sersic indices) tend to have the most luminous and spatially extended nuclei (although the trend between \(n\) and \(\eta\) is statistically significant
only when an unweighted fit is used). These trends are generally consistent with an increasing importance for gas dissipation as one moves to increasingly higher mass galaxies. Nuclei formed through merger-driven gas inflow could also be expected to follow a mass–radius scaling relation, as Hopkins & Quataert (2010) found that stellar systems may have a maximum stellar surface density, due to feedback from massive stars. One complication with the gas inflow model is that it obviously requires the presence of gas, which is not consistent with the “classical” picture of early-type galaxies. However, both low-mass Es and high-mass “dEs” are now recognized to be quite complex, having been found to contain dust, spiral arms, embedded disks, and bars (Jerjen et al. 2000; Barazza et al. 2002; De Rijcke et al. 2003a; Lisker et al. 2006b; Ferrarese et al. 2006b), as well as counter rotating and kinematically decoupled cores (De Rijcke et al. 2004; Thomas et al. 2006; Chilingarian et al. 2008), and ongoing star formation (e.g., De Rijcke et al. 2003b; Lisker et al. 2006a; Côté et al. 2006; Michielsen et al. 2007). These features suggest that a non-negligible fraction of intermediate-mass galaxies classified as “early” types has experienced some level of morphological transformation, likely through mergers, accretions, or interactions with the cluster environment (Moore et al. 1996; Kazantzidis et al. 2011).

It is, in fact, possible that the nuclei in some of our early-type galaxies formed in late-type progenitors. A recent finding by Emsellem & van de Ven (2008) noted that galaxies with Sersic indices of $n \lesssim 3.5$ have compressive tidal forces in their central regions, with the size of the compressive region increasing with a decreasing Sersic index. Assuming a constant Sersic index of $n = 1$, the amplitude of the tidal forces was found to scale linearly with galaxy mass and form a CMO with a constant host mass fraction of $\sim 0.5\%$. A CMO growing through gas accretion in this way would eventually reach a critical density and luminosity, altering the galaxy profile such that it no longer has central compressive forces. A comparison of this theoretical threshold of nucleus luminosity with C06 reveals that many of the observed nuclei are much more luminous than would be predicted by this model, which suggests that the nuclei in early-type galaxies may have formed in some low-Sersic index, gas-rich progenitors that have since evolved morphologically.

High-resolution observations of the molecular and neutral hydrogen in these galaxies may be able to constrain the role of gas inflow and enrichment in nucleus formation, since H$_2$ will highlight regions of star formation, while H$^+$ is a tracer of processes affected by the ICM and gravitational interactions. Subarcsecond-resolution maps of molecular starburst gas—using ALMA to observe the CO transitions and EVLA to detect H$^+$ through 1.4 GHz emission—would allow the relationship between galaxy nuclei and molecular gas to be examined in much greater detail than is currently possible.

4.3.3. Possible Connections to Black Holes

As discussed in Section 1, recent observations have uncovered the coexistence of nuclei and black holes in intermediate-mass galaxies, which may have implications for the evolution of the central regions of galaxies. For instance, Hopkins & Quataert (2010) performed simulations of gas accretion onto a black hole, which they find can form a lopsided, eccentric nuclear disk that exerts a strong torque on and drives in the remainder of the gas, producing a system much like that found in M31.

The density of the central nucleus remnant in the analytical cluster merger model of Antonini 2012 was found to decrease with the addition of a central black hole. Additionally, simulations by Bekki & Graham 2010 examined the merging of two nuclei containing black holes, and found the dynamical heating of the cluster from the black hole binary expelled stars from the center, with the final stellar density of the remnant decreasing with increasing black hole mass fraction. This type of merger could produce observed “core” galaxies with larger black holes (as originally noted by Ebisuzaki et al. 1991; see also Milosavljević & Merritt 2001) and shape the inner regions of intermediate-luminosity galaxies in which a nucleus is difficult to distinguish observationally (Section 4.1.1). Bekki & Graham 2010 further showed that if only one nucleus had a black hole, the decrease in stellar density of the nucleus was less pronounced, as most of the heating comes from the black hole binary. In mergers where neither nucleus had a black hole, the stellar density of the nucleus increased.

If black holes do become an increasingly dominant component of the CMO mass budget in high- and intermediate-luminosity galaxies, then they could either hinder nucleus growth or lower the density of the nucleus through mergers until it is destroyed by black hole binary feedback. These effects could create the trends in the intermediate-mass galaxy surface brightness profiles observed in this study, where the galaxies undergo a transition from central light “excesses” to “deficits” as they become more luminous (see also Paper IV).

5. SUMMARY

This HST study examined 43 early-type galaxies in the Fornax cluster, imaged in the ACS F475W and F850LP bands. Our analysis—performed in both one and two dimensions—extracted photometric and structural parameters for 31 compact
stellar nuclei in these early-type galaxies. The main results are summarized as follows.

1. We have compared our 1D results to those obtained by using 2D image modeling techniques and found the extracted nucleus structural parameters to be in agreement for both methods. Although 2D fitting potentially allows for the full structural decomposition of a galaxy, 1D methods enable characterization of the outer regions with a single surface brightness profile. We conclude that 1D fits are more appropriate for our study, since they allow us to easily compare nucleus and galaxy parameters in an objective and homogeneous way.

2. We find that 72% ± 13% of the 43 galaxies in our sample are nucleated, which is a significant increase from ground-based studies. The nuclei—defined as a central excess relative to the inward extrapolation of a Sersic model (C06)—are found exclusively in galaxies with $M_B \gtrsim -19.5$ (M$_\star \lesssim 10^{10.6}$M$_\odot$), and the frequency of nucleation for galaxies fainter than this magnitude is 89% ± 16% (31/35). As found previously in the Virgo cluster, nuclei are exceedingly common in low-mass, early-type galaxies in the Fornax cluster (i.e., M$_\star \gtrsim 10^{9}$M$_\odot$).

3. Most nuclei are not significantly offset from their host photocenter—only three are offset by more than 0.5”. We do not find any trend between the magnitude of the offset and host galaxy luminosity.

4. We find a nearly constant nucleus-to-galaxy luminosity ratio of ≈0.4%. The observed nucleus luminosity function can be understood therefore in terms of the galaxy selection function (and the fact that galaxies brighter than $M_B \lesssim -19.5$ do not contain nuclei). If we parameterize the nucleus luminosity function as a normalized Gaussian, we find peaks at $\langle M_g \rangle = -11.5$ and $\langle M_z \rangle = -12.7$ mag, which is ~40 times more luminous than the peak of the GC luminosity function. The nuclei are also found to have larger sizes and different effective surface brightness scaling relations than the GCs.

5. The colors of the nuclei in hosts with $B_T < 13.5$ are found to correlate with galaxy colors, as well as with galaxy and nucleus luminosities. In particular, both the galaxies and the nuclei were observed to become increasingly red with increasing galaxy luminosity, with the trend being steeper for the nuclei. This leads to a relation between nucleus-and-host color difference and host magnitude, where nuclei that are redder than their hosts are found predominantly in brighter galaxies, and vice versa. However, on average most of the nuclei are significantly bluer in $(g - z)$ color than their hosts by 0.28 ± 0.04 mag.

6. A comparison to C06, which examined the nuclei of early-type galaxies in Virgo, reveals many similarities between the nuclei in the two environments. Both studies find similar frequencies of nucleation (increasing sharply from 0% to ≳70% for galaxies with $M_B > -19.5$ mag), surface brightness selection effects, nucleus-to-galaxy luminosity ratios, nucleus luminosity functions, sizes, and color–magnitude relations. The trend along the luminosity function where the galaxy central surface brightness profiles gradually change from having a luminosity “deficit” to an “excess” is shared by both samples (see also Paper II; Paper IV), which suggests that generic formation and evolution processes largely independent of the galaxy environment are involved in shaping the central regions of galaxies. Rather, nucleus cre-

ation may be more contingent on local factors, especially host galaxy mass.

Our conclusion is that, in low-mass galaxies, the dominant mechanism for nucleus growth is probably infall of star clusters through dynamical friction, while at higher masses, gas accretion resulting from mergers and torques becomes dominant. There is no reason to expect either of these processes to be discontinuous, and we argue that the relative importance of these processes vary smoothly as a function of galaxy mass.

We examine the efficiency of dynamical friction in our sample galaxies and confirm the finding of many previous studies that star cluster infall is most effective in low-mass galaxies. Based on simulations carried out by other researchers, we argue that gas infall, followed by central star formation, becomes increasingly important in high-mass galaxies having Sersic indices that may have been inflated by successive mergers and accretions.

There is also some evidence for “hybrid nuclei” in some of the intermediate-mass galaxies in our sample, i.e., nuclear components with complex inner structures. Simulations that take into account multiple formation mechanisms—star cluster infall, gas accretion driven by tidal torques and/or accretions and mergers, the influence of central black holes, etc.—are urgently needed to elucidate the processes that drive nucleus formation in different mass regimes.

Both dissipationless cluster infall and gas accretion models make predictions that nucleus formation would depend on local density (Oh & Lin 2000; Babul & Rees 1992). Although the fact that we do not find any major differences between the nuclei of Virgo and Fornax suggests that local density may not be a dominant factor in their formation, observations that examine the entire volume of a galaxy cluster (and that have the sensitivity necessary to detect the nuclei) may help determine the role environment plays in shaping the nuclei and their hosts. In this context, the forthcoming Next Generation Virgo Cluster Survey (L. Ferrarese et al. 2012, in preparation), which is imaging the entire Virgo cluster to a (10σ) depth of $g \approx 25.7$, should provide important new constraints on formation models.

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Facility: HST(ACS)
Figure 21. Upper row: F475W image for FCC 190 displayed at three different intensity stretches (A, B, and C) and two different magnifications (A/B vs. C). Note the prominent nucleus visible in panel (a), and the dramatic changes in ellipticity and position angle with radius. Panels (d) and (e): Galaxy model constructed using ellipse, with contours overlaid to illustrate the gradual changes in galaxy flattening and orientation. Panels (d) and (e): residual image (observed − model) showing a weak residual bar, with a peak intensity of ~0.02 e−1, corresponding to $\mu_g \sim 23.8$ mag arcsec−2.

APPENDIX
COMPARISON WITH TWO-DIMENSIONAL SURFACE BRIGHTNESS PROFILE FITTING

Section 2 describes the determination of nucleus parameters through 1D fitting of surface brightness profiles from ellipse. This appendix examines the pros and cons of 1D and 2D methods when measuring parameters for the photometric and structural parameters of nuclei in early-type galaxies.

In general, the decision to use a 1D or 2D approach depends on the specific scientific goals. If a galaxy has multiple components (which even for early-type galaxies can include, e.g., bulges, large-scale disks, embedded disks, outer/inner rings, bars, shells, dust filaments, dust disks, and even faint spiral arms), then, by using 2D decomposition, individual structure can, in principle, be fitted with separate profiles and the galaxy’s composition examined in detail. The 2D fitting program GALFIT (Peng et al. 2002, 2010) allows the implementation of many surface brightness profile modifications, such as variability of their diskiness/boxiness, or the addition of spiral arms and non-axisymmetric bending modes—an attractive feature of the 2D method. However, full galaxy decomposition is, in practice, not always straightforward, particularly for nearby galaxies observed at HST/ACS resolution. In many situations, it is not clear how many components are needed to fully fit a galaxy, and the physical origin of each component may not be obvious. For example, sometimes multiple surface brightness profiles are required to fit what may be the same photometric component (see Peng et al. 2002 for examples) due to the fact that the models used in 2D methods have fixed center, ellipticity, and position angle, and have difficulty characterizing a galaxy profile in which these parameters are not intrinsically constant on all scales.

The method of 1D profile fitting used in this work, however, allows the aforementioned parameters to vary, and we are therefore usually able to cleanly fit an entire galaxy with a 1D model. A demonstration of this is shown in Figure 21, where we examine the structure of FCC 190 (panels (a)–(c)) and plot the ellipse model derived from our fitted elliptical isophotes (panels (d) and (e)). This figure illustrates the striking change in the shape of this galaxy’s isophotes when moving from small to large scales, and how this effect is well captured by the model. The residuals of the fit (panel (f)) are relatively clean and reveal a weak ($\mu_g \sim 23.8$ mag arcsec−2) central bar. To compare to
a 2D fit, the inner $10 \times 10^\prime$ residuals from fitting 1S and 2S profiles to FCC 190 using GALFIT are shown in Figure 26(a). Clearly, two Sersic profiles with fixed ellipticity and position angle are unable to fully parameterize this galaxy. However, the penalty in this approach is that the information about the shapes, sizes, and relative position angles of various galaxy components is lost, as their surface brightness profiles blend together into a single component which describes the galaxy on global scales.

Our study is concerned with the properties of the nuclei in comparison to their host galaxies, and with the global trends in these properties as a function of galaxy luminosity or mass. Thus, we are not interested in a full decomposition of any large-scale galaxy structure; rather, we are seeking to characterize the main galactic body component as a whole, so 1D techniques are most appropriate for our study. However, it is important to ensure that the nucleus structural parameters extracted using 1D methods are robust. To test this assertion, we perform surface brightness profile fitting in 2D and compare the results obtained using the two techniques.

A.1. Procedure

To perform our 2D analysis, we use GALFIT (Peng et al. 2002, 2010), a program that fits galaxy images using multi-component 2D intensity profiles, using an iterative downhill gradient Levenberg–Marquardt algorithm. This 2D analysis is performed on all galaxies in our sample with $B_T \gtrsim 13.5$, a cutoff which was chosen to include most of the nucleated galaxies, while avoiding those that are much more challenging to fit in either 1D or 2D. Galaxies brighter than this are known to show a complex structure, regardless of their classification as Es, S0s, dEs, or dS0s. For instance, some of the brighter dEs are known to show substructures including disks, spiral arms, and bars (e.g., Lisker et al. 2006b, 2007). Likewise, more massive galaxies—often classified as Es and S0s—frequently show similar morphological complexities (see, e.g., Bender & Moellenhoff 1987; Combes et al. 1990; Nieto et al. 1992; Scorza et al. 1998; Ferrarese et al. 2006b; Krajnovic et al. 2011). The substructures identified in these early-type galaxies could either be a sign that they are intrinsically more complex objects or a selection effect arising from their higher luminosities and surface brightnesses, which aid in the detection of these distinct components. In any case, the sample of galaxies used in our 2D analysis consists of 27 galaxies, 24 of which are found to be nucleated in our 1D analysis. This sample includes roughly equal numbers of galaxies listed in Table 2 of Paper I as “giants” (E/S0) or “dwarfs” (dS0, dE, etc.), although such classifications should be viewed with caution since there can be significant discrepancies among classifiers: see, e.g., Chen et al. (2010) and Paper III where issues relating to the morphology of ACSVCS and ACSFCS galaxies are explored in more detail.

Our analysis proceeded by first measuring the background sky value. To do so, we used SExtractor to mask out any background sources, and then convolved this mask with a Gaussian in order to thoroughly cover any diffuse outer edges. The galaxy was then masked with an ellipse of geometric radius length between five and six effective radii (determined from the 1D analysis). We then used the biweight value of the remaining pixels as the sky value for each of the four ACS chips. Although the sky value between different chips was found to vary up to $\sim1$ count, we found that such a count difference resulted in no more than 5% difference in any of the fitted parameters; we therefore adopted the average of the biweight estimates for each of the four chips as the sky value.

We began by fitting each galaxy with a single Sersic (S1) profile. We then attempted to fit each of the 24 galaxies classified as nucleated in 1D by adding a second Sersic component (for the central nucleus). In 13 cases, it was possible to fit the nucleus with a Sersic model with all fit parameters varying freely. Five more galaxies required a prior on the nucleus Sersic index which was fixed at $n = 2$ in analogy with Galactic GCs. For the six remaining galaxies, GALFIT was not able to converge on a nucleus with only one Sersic component fitted to the main body of the galaxy; at least one other large-scale component needed to be added for before a fit to the nucleus could be achieved. However, in one case (FCC 43) the nucleus parameters were flagged as having caused numerical convergence issues, and thus we do not include the $S \gtrsim 2$ fit in our results. In all cases, we did not impose any constraints on the relative position angles of the fitted components.

The above procedures are summarized in Figure 22, where we have plotted the 1D versus 2D magnitudes, Sersic indices, and effective radii for the galaxies and nuclei from our sample. For the galaxies that require more than two Sersic components to fit the nucleus, we use the parameters from our 2D S1 fit to plot the galaxy portion. Although the galaxy main body (filled black circles) parameters are generally in good agreement from both techniques, we note a slight offset in effective radius, where those obtained from the 2D fits are usually somewhat smaller than in 1D (by a factor of $0.94 \pm 0.02$, derived from least-squares fit, with a fixed line slope of 1, to the galaxy main body effective radii in the log). The S2 nuclei (filled blue squares) are also relatively consistent between techniques, although with some notable outliers that will be discussed below. Finally, the non-S2 nuclei (magenta open squares) appear to show the most scatter. We note that the scatter in nucleus magnitudes appears to be the most significant for the brightest nuclei, probably due to the increased difficulty of extracting nucleus parameters from structurally complex galaxies that often have high central surface brightness. This can be seen clearly in Figure 23, where we have plotted the magnitude differences as a function of 1D magnitudes. We now discuss findings for galaxies in these different categories.

A.2. Non-nucleated Galaxies (S1)

There are three galaxies in our 2D sample where we do not find a nucleus in our 1D analysis, a result with which we find full agreement in 2D. It is interesting to examine the residuals of a single-Sersic fit to these objects individually to determine why they are not found to be nucleated, since it is the lack of a nucleus that is unusual for galaxies in our sample.

The residuals of FCC 152 (Figure 24(a)) reveal large amounts of dust, but with no nucleus-like object present in the central regions. FCC 143 (Figure 24(b)) shows a small bar in the residuals, which appears to have a bright excess in the center. Nevertheless, even with the addition of one or two more large-scale Sersic profile components, GALFIT is unable to fit a central nucleus. Finally, the low-mass galaxy FCC 26 (Figure 24(c)) has two bright compact objects located 0′95 and 1′37 away from the galaxy photocenter. However, it is unclear if either of these objects in this actively star-forming, “dE/dIrr transition” galaxy can unambiguously called a true “nucleus.”

19 Performing a 1D fit to the residuals, we find $R_e \sim 0′02$ and $g \sim 20.19$ mag for the inner and $R_e \sim 0′22$ and $g \sim 20.63$ mag for the outer component.
Figure 22. Top left: values for nucleus g-band luminosity obtained from the 1D and 2D fits (ordinate and abscissa, respectively). The filled blue squares show the host galaxies, the filled black circles indicate the nuclei from galaxies fit well by an S2 profile in 2D, and the filled magenta circles represent the nuclei belonging to galaxies in which more than two Sersic components (i.e., $S > 2$) were required in 2D. The dotted red line is the relation where the parameters obtained from both methods are equal. Galaxies and nuclei where the measured magnitudes differ by more than 0.5 mag between methods are labeled. The root-mean-squared (rms) error around the magnitude sample mean is shown for the galaxies, nuclei, and nuclei again after applying 3σ clipping. Top right: same as the top left, except for Sersic indices. Galaxies and nuclei where the measured Sersic indices differ by more than 1.0 between methods are labeled. We note that labels for the blue filled squares are to the left of the points, while those for the magenta open squares are to the right. Bottom: same as top, except for galaxy (left) and nucleus (right) geometric mean effective radii. Galaxies and nuclei where the measured effective radii in 1D and 2D differ by more than 0.1 in the log are labeled. The black dashed line shows the best-fit line to the galaxy effective radii, with a fixed slope of unity. (A color version of this figure is available in the online journal.)

A.3. Nucleated Galaxies Fit with Double-Sersic Profiles (S2)

Of the 23 nucleated galaxies in our 2D sample, we are able to fit the galaxy and nucleus using an S2 profile for 18 systems. The residuals from the S1 and S2 fits to these galaxies are shown in Figure 25, where the galaxies are displayed in order of increasing blue magnitude from the FCC. This figure illustrates how the structural complexity of the galaxies seems to increase, and then diminish, as their luminosity decreases—reaching an apparent maximum in the range $-19 \lesssim M_B \lesssim -17$ or $10^{10.4} \lesssim M_*/M_\odot \lesssim 10^{9.6}$—with the residuals for the faintest galaxies appearing much cleaner (see Ferrarese et al. 2006b; Lisker et al. 2006b). Of course, part of this apparent simplicity is likely related to the lower S/N of the available imaging for the faintest and lowest surface brightness systems.

For five of the S2 galaxies, the Sersic index of the nucleus needed to be held fixed during the fit. FCC 190 (Figure 25(a)), FCC 55 (Figure 25(d)), FCC 95 (Figure 25(e)), and FCC 136 (Figure 25(g)), all have substructure such as bars that overlap with the nuclear region which the second Sersic component attempts to fit. By fixing the Sersic index of the nuclei at $n = 2$ (appropriate for Galactic GCs), GALFIT is able to fit the nucleus, with the resulting magnitude and effective radius of the nucleus in agreement with the 1D results in all cases except for FCC 190, which is discussed below. The other galaxy that requires a fixed nucleus Sersic index, FCC 335, contains a large amount of dust in the central regions, and if the nucleus...
Figure 24. Panel (a): GALFIT residuals from an S1 model fitted to FCC 152, showing the inner 10′′ × 10′′ region. Panels (b) and (c): same as for panel (a) but for FCC 143 and FCC 26.

Figure 25. Panel (a): GALFIT residuals from S1 (left) and S2 (right) models fitted to FCC 190, showing the inner 10′′ × 10′′ region. These results should be compared to the e11pae model (1D) results shown in Figure 21. Panels (b)–(r): Same as for panel (a) but for the galaxy labeled. Galaxies have been ordered by increasing blue magnitude (decreasing luminosity) from the FCC.
Sersic index is allowed to vary, then the nucleus effective radius and Sersic index converge to very small values that GALFIT warns may cause numerical convergence issues which cause the final solution to be unreliable. The differences between the 1D and 2D results for this galaxy are also discussed below, where we describe nuclei that are notable outliers in Figure 22. Specifically, the nuclei of FCC 190, FCC 335 and FCC 90 have 1D and 2D magnitude differences of \( >0.4 \) mag and fractional differences in their effective radii of \( >0.5 \).

**FCC 190.** This nucleus is 0.55 mag brighter and twice as large in effective radius in the 2D fit than in 1D. The galaxy exhibits distinct “peanut-shaped” residuals, as shown in Figure 25(a). It should be noted that after fitting both a bulge and a disk component along with the nucleus, the nucleus magnitude and radius are still notably disparate.

**FCC 335.** In 2D, the nucleus is 0.42 mag brighter, but four times smaller, than in the 1D fit. The 2D residuals are shown in Figure 25(e). This galaxy has a large amount of dust, and the center was held fixed during the ellipse fitting for the 1D analysis. However, the position of the 1D fit ellipse center is actually \( \sim 0.5 \) pixels away from the nucleus (as determined by GALFIT and confirmed by eye). This could cause the
The Astrophysical Journal Supplement Series, 203:5 (33pp), 2012 November

Turner et al.

A.4. Nucleated Galaxies with Multiple Large-scale Components (S > 2)

There are six nucleated galaxies in our sample which we were unable to model in 2D using an S2 model, as a second Sersic component in GALFIT will, even with its Sersic index held fixed, attempt to fit a different component of the underlying galaxy. Thus, we need to add a second, or even third, Sersic component to the main body of the galaxy in order to fit the nucleus (i.e., three or four components in total). A comparison of the 1D and 2D nucleus parameters for these six galaxies is given in Table 7. Note that the nuclei in several of these galaxies are candidates for “hybrid nuclei” with a complex structure (e.g., a compact, high surface brightness component embedded in a small-scale disk-like feature) that are suggestive of multiple, parallel formation processes (see Sections 4.3.1 and 4.3.2).

| FCC | $s_{AB}$ (mag) | $R_e$ (arcsec) | n | 1D | 2D | 1D | 2D | 1D | 2D |
|-----|---------------|----------------|---|-----|-----|-----|-----|-----|-----|-----|
| 310 | 18.6          | 18.5           | 0.36 | 0.46 | 1.4 | 2.0 |
| 249 | 20.1          | 19.0           | 0.04 | 0.09 | 2.0 | 2.0 |
| 148 | 16.4          | 18.0           | 0.27 | 0.05 | 4.0 | 2.2 |
| 301 | 20.3          | 20.0           | 0.02 | 0.03 | 1.0 | 1.1 |
| 204 | 20.0          | 20.4           | 0.09 | 0.04 | 4.0 | 2.0 |

Table 7
1D and 2D Nucleus Parameters for Multi-Component (S > 2) Galaxies

FCC 43. A small (∼10″ in diameter) round central component seen in Figure 26(a) needs to be fitted before it is possible to fit to the nucleus. However, because of the small size of the fitted nucleus (i.e., an effective semimajor axis of 0.39 pixels), the output of GALFIT indicated that this parameter may have caused numerical convergence issues, making all parameters from this solution unreliable. We therefore did not include these results in Figure 22.

FCC 310. After fitting with a single Sersic profile, the bar and outer envelope-like structure of this galaxy become apparent from the residuals, seen in Figure 26(b). To fit the nucleus, we must first fit an $n = 2.38$ bulge-like component, an $n = 0.26$ bar, and an $n = 0.20$ outer envelope. After these three components are fit, the nucleus appears quite clearly in the residuals, and it can be fitted by adding a fourth Sersic profile with its Sersic index held fixed at $n = 2$.

FCC 249. A single-Sersic fit reveals a peanut-shaped residual in the center (Figure 26(c)), with a possible nucleus. After a second small component is added, a nucleus becomes apparent in the residuals. The nucleus can then be fitted with its Sersic index held fixed at $n = 2$.

FCC 148. This galaxy shows a very boxy inner bulge, with X-shaped isophotes in intermediate regions (Figure 26(d)). Since we are unable to fit the host and nucleus with a double-Sersic model, a second large-scale component with disk-like properties ($n = 1.04$ and an axis ratio of 0.36) is added, after which GALFIT will converge on the nucleus. Although a nucleus is not very prominent in the two-component fit residual, the Sersic index of the bulge-like component grows to $n = 9.35$ if a nucleus is not included in the fit. After a nucleus is included, the fitted bulge Sersic index is $n = 5.1$. The disk-like component does not change significantly with the addition of the nucleus.

FCC 301. The complex structure of this galaxy, seen in the single Sersic component fit residuals in Figure 26(e), can be appreciated from the 1D surface brightness profile (Figure 3), where the intensity is slightly oversubtracted at 1″, and then undersubtracted out to ∼5″. There are also bright outer wings, at >10″ scales. After a single-Sersic component is fitted, a second component will converge on the larger bright central excess, and a third Sersic profile will then fit the nucleus. However, the bright residuals show that the main body of this galaxy is not well described in 2D, even by two Sersic profiles.

FCC 204. As is the case for FCC 43, there appears to be an embedded disk in this galaxy, which can be seen in the residuals of a single Sersic fit, Figure 26(f). The nucleus is found to be slightly fainter in the 2D fit than in 1D. It is possible that in 1D, the central disk might be contributing to nucleus component and causing the nucleus luminosity to be overestimated.

Overall, the 2D nucleus parameters from these complex galaxies are in reasonable agreement with those found in the
1D analysis. In terms of magnitude, only FCC 148 and FCC 249 show differences of >0.5 mag, although all except for FCC 310 show discrepancies of >50% in effective radius and Sersic index. However, the differences do not appear to be systematic, in the sense that there does not seem to be consistent under or overestimation of a specific parameter in 1D or 2D. The nucleus parameters for these cases are likely to be more uncertain overall, and thus larger differences between the extracted parameters in these structurally complex galaxies are to be expected.

A.5. Nucleus Ellipticities

One advantage of performing the 2D analysis is that we are able to measure the nucleus ellipticities. In general, we find the nuclei to be flattened, with median ellipticities of 0.20 and 0.25 for the full and only S2 samples, respectively. The top right panel of Figure 27 shows a histogram of the ellipticity distribution, while in the top left panel, we plot ellipticity against host galaxy magnitude. A least-squares fit to all of the nuclei hints at a trend of increasing nucleus ellipticities with galaxy luminosity,

\[ \epsilon_{\text{nuc}} = -(0.062 \pm 0.027) B_T + (1.2 \pm 0.40), \quad (A1) \]

and after removing the more uncertain \( S > 2 \) nuclei, we obtain a significant relation:

\[ \epsilon_{\text{nuc,S2}} = -(0.10 \pm 0.03) B_T + (1.8 \pm 0.45). \quad (A2) \]

This result suggests that nuclei in brighter (and higher mass) galaxies are more flattened, and may be more likely to contain edge-on disk-like components.

In the bottom panel of Figure 27, we show nucleus ellipticities versus the difference in position angle between the nuclei and their host galaxies. We find that the most highly flattened nuclei are aligned with their hosts, although over one-third (7/18) of our sample are significantly (\( \Delta P.A. > 20 \) deg) misaligned.

A.6. 2D Analysis Conclusion

Figure 22 shows that there is reasonable agreement between the nucleus parameters measured in 1D and 2D. We conclude that the 1D nucleus parameters are for the most part robust, and note that the brightest and most structurally complex galaxies—which typically have \( \mu_s(1') \lesssim 19 \) mag arcsec\(^{-2}\)—present a challenge for measuring nucleus parameters using either approach. Indeed, even in cases where adding a second or third profile to the main body is required to fit the nucleus in 2D, it is unclear how many components must be added until a “best” fit is actually achieved, and it is usually difficult to say whether one method yields parameters closer to those of the true nucleus. In our study of Fornax nuclei, we are primarily interested in extracting the nucleus parameters relative to the average outer profile. Although much of the power of 2D techniques lies in their ability to fit multiple large-scale components, in galaxies that require more than one outer Sersic profile, it becomes more difficult to perform a fully objective and homogenous comparison between the nuclei and galaxy parameters. Our analysis therefore uses the results from our 1D fits, which meets the dual criteria of objectivity and homogeneity. The general consensus between methods indicates that the main conclusions in this work are independent of the specific approach used to model the galaxies and their nuclei.
