Instance Influence Estimation for Hyperspectral Target Signature Characterization using Extended Functions of Multiple Instances

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ABSTRACT

The Extended Functions of Multiple Instances (eFUMI) algorithm is a generalization of Multiple Instance Learning (MIL). In eFUMI, only bag level (i.e., set level) labels are needed to estimate target signatures from mixed data. The training bags in eFUMI are labeled positive if any data point in a bag contains or represents any proportion of the target signature and are labeled as a negative bag if all data points in the bag do not represent any target. From these imprecise labels, eFUMI has been shown to be effective at estimating target signatures in hyperspectral subpixel target detection problems. One motivating scenario for the use of eFUMI is where an analyst circles objects/regions of interest in a hyperspectral scene such that the target signatures of these objects can be estimated and be used to determine whether other instances of the object appear elsewhere in the image collection. The regions highlighted by the analyst serve as the imprecise labels for eFUMI. Often, an analyst may want to iteratively refine their imprecise labels. In this paper, we present an approach for estimating the influence on the estimated target signature if the label for a particular input data point is modified. This instance influence estimation guides an analyst to focus on (re-)labeling the data points that provide the largest change in the resulting estimated target signature and, thus, reduce the amount of time an analyst needs to spend refining the labels for a hyperspectral scene. Results are shown on real hyperspectral sub-pixel target detection data sets.

Keywords: eFUMI, interactive labeling, influence, target proportion, residual error

1. INTRODUCTION

The Extended Functions of Multiple Instance (eFUMI) algorithm is a hyperspectral target characterization method that estimates the spectral signature of a target of interest from training data with imprecise and uncertain labels. The eFUMI algorithm addresses problems that are generalizations of those addressed by a standard Multiple Instance Learning (MIL) framework. In MIL, the training points are grouped into “bags.” A bag is a multi-set of training data points. Each bag is labeled as “positive” or “negative.” Under MIL, positive bags are assumed to contain at least one target data point and negative bags contain exclusively non-target points. Generally, MIL algorithms assume that each data point is either entirely a target or a non-target data point. The eFUMI algorithm extends the MIL framework to address data points that are mixtures of target and non-target signatures. Thus, in eFUMI, positive bags are assumed to contain at least one data point that has some non-zero proportion of target. Negative bags in eFUMI are assumed to contain data points that all have zero target proportion.

The advantage of MIL and eFUMI during hyperspectral image analysis is that they allow for bag-level (instead of precise instance-level) training labels. Creating bag level labels is generally much less time consuming and, often, much more feasible than assigning accurate data-point level training labels. For example, in the case of sub-pixel target detection in remotely-sensed hyperspectral imagery, GPS coordinate of targets in training data may be known but the accuracy of the GPS coordinates may range across several pixels. Thus, the ground truth
in this case is inherently imprecise. Yet, it is feasible from this imprecise ground truth data to create positive bags associated with each ground truth point and include all pixels in a neighborhood based on the GPS unit accuracy and, also, create negative bags which are far from all GPS target ground truth points.

Another scenario in which eFUMI may be useful is one in which an analyst circles regions of interest in an image (and, thus, these regions become positive bags) and also circles regions of no-interest (these become negative bags). Then, eFUMI can take these regions and produce an estimate of the target spectral signature that is found in all positive bags (and not found in any negative bags). By being able to circle general regions of interest using some sort of user interface, it is much more intuitive and easier for an analyst to generate label maps as opposed to being required to create some sort of pixel level label maps.

However, differences in labeling may cause differences in the eFUMI result. Thus, after obtaining an eFUMI result, an analyst may wish to refine their bags and bag-level labels. In this paper, we propose two methods for identifying which pixels (or image regions) would cause the largest change in eFUMI results if relabeled. Our two proposed influence estimation methods estimate the relative degree that the resulting eFUMI-estimated target endmember will change after changing the labels of the respective pixels/regions.

2. EXTENDED FUNCTIONS OF MULTIPLE INSTANCES

The eFUMI algorithm is a method to learn a target signature from training data without the need of instance-level labels. Specifically, the goal of eFUMI is to estimate a target signature, $e_T$, non-target signatures, $\{e_k\}_{k=1}^M$, the number of needed non-target signatures, $M$, and the function parameters, $p_i$, which define the relationship between each data point, $x_i$, and the endmember signatures. These are estimated given a set of input training data, $\{x_i\}_{i=1}^N \in \mathbb{R}^D$ which have been partitioned into $K$ “bags,” $B = \{B_1, \ldots, B_K\}$, with associated bag-level labels, $L = \{L_1, \ldots, L_K\}$. Each training point is assumed to be a function of target and non-target signatures, $x_i = f(E_i, p_i)$. In the results shown here, we consider the case of a convex combination for the functional form, $x_i = p_{iT}e_T + \sum_{k=1}^{M} p_{ik}e_k$ subject to the constraints that $p_{iT} + \sum_{k=1}^{M} p_{ik} = 1$, $p_{iT} \geq 0$, $p_{ik} \geq 0$, $\|e_k\|^2 = 1$, and $\|e_T\|^2 = 1$. Furthermore, the bag-level labels are unspecific since, if for bag $B_j$ with $L_j = 1$ (thus, $B_j$ is a positive bag), this indicates that there is at least one data point in $B_j$ with a positive $p_{iT}$ indicating some presence of target, as in (1), where $\varepsilon_i$ is an error term.

$$\text{if } L_j = 1, \exists x_i \in B_j \text{ s.t. } x_i = p_{iT}e_T + \sum_{k=1}^{M} p_{ik}e_k + \varepsilon_i, \ p_{iT} > 0 \quad (1)$$

However, the exact number of data points in a positive bag with a target contribution (i.e., $p_{iT} > 0$), is unknown, also, the target proportion is unknown. Furthermore, if $B_j$ is a negative bag (i.e., $L_j = 0$), then this indicates that none of the data in $B_j$ contain any target, as in (2).

$$\text{if } L_j = 0, \forall x_i \in B_j, x_i = \sum_{k=1}^{M} p_{ik}e_k + \varepsilon_i \quad (2)$$

Given training data of this form, instance-level labels are unknown. eFUMI addresses this problem using an Expectation Maximization (EM) approach in which the instance-level labels are the hidden, latent variables in the EM model. The assumed complete data log-likelihood is proportional to a cost function with an approximation error term (minimizing the L2 norm between training points and eFUMI-estimated reconstructed per-point signatures), endmember constraint terms (minimizing the L2 norm between endmembers and global data mean) and a sparsity promoting term (promoting the proportions associated with unnecessary endmembers to be zero). The optimization of the cost function is solved by iteratively via EM. Since instance-level labels are unknown for each training point, in the E-step, the conditional probability of an instance-level label given parameters and bag-level label is computed. In the M-step, estimated endmembers and proportions are updated by minimizing the expected value of cost function with respect to the latent instance-level label. The cost function is iteratively minimized until some stopping criterion is reached. Full details of the eFUMI algorithm can be found in the paper by Jiao and Zare.
3. PROPOSED METHOD

Given the eFUMI algorithm outlined in the previous section, our goal in this paper is to estimate the influence of each pixel or an image region on the result of the eFUMI algorithm. Specifically, our goal is to estimate which pixels would cause the largest change in the target spectral signature estimated by eFUMI if their labels were switched. By identifying which pixels would cause the largest change in the eFUMI algorithm, then one could guide an analyst to focus on (re-)labeling only those pixels that would have a significant influence on the eFUMI result. Hopefully, this would result saving analyst time and effort during analysis.

Given the goal of determining which pixels cause the largest change in the estimate target spectral signature, we define influence of a pixel as:

\[ I_i = \| e_t - e_{t,i} \|^2 \]  

(3)

where \( e_t \) is the estimated target endmember without changing any label values (i.e., the target estimation result using an initial set of bag-level labels) and \( e_{t,i} \) is the estimated target endmember after changing the label of point \( x_i \) (i.e., switching the label to be “negative” to “positive” or vice versa. One could certainly determine influence of each pixel by laboriously switching the label of each pixel in series, re-running eFUMI for the modified label set, and computing the resulting change in the estimated target signature. However, this would be extremely time consuming and, thus, infeasible for the development of an interactive method for hyperspectral unmixing analysis.

Therefore, this article proposes two fast methods to approximate the relative influence of a single point or image region (e.g., a superpixel). Both of the proposed methods extremely reduce the time needed to estimate relative influence as compared with original relabeling-re-running process for each point/superpixel. Instead, only running eFUMI once is necessary. After running eFUMI with initial user-selected labels, the first proposed method estimates relative influence by applying the fully-constrained least-squares unmixing algorithm to all data points using the endmembers estimated from the initial run. Then, we propose to use the target proportion value estimated for each point as a surrogate for the influence measure. Namely, for each point \( x_i \), we find:

\[ p_i = \arg \min_{p_i} \| x_i - E p_i \|^2 \]  

(4)

\[ \text{s.t.} \quad \begin{cases} 
  p_{ij} \geq 0 & \forall i, j \\
  \sum_{j=1}^{M+1} p_{ij} = 1 & \forall i, j
\end{cases} \]  

(5)

where \( E \) is a matrix containing the estimated endmembers, \( p_i \) is the proportion vector for point \( x_i \), \( p_{ij} \) is the proportion value of endmember \( j \), and \( M \) is the number of non-target endmembers. The surrogate influence measure is set to \( p_{it} \), the proportion value estimated for the target endmember for the \( i^{th} \) data point. This method identifies the data points with large target portion. Thus, changing the label of these data points would have a large influence of the resulting estimated target endmember.

For the second proposed method, given the estimated endmembers and proportions for each point, the residual error is computed:

\[ r_i = \| x_i - E p_i \|^2 \]  

(6)

where \( E \) is the estimated endmembers, \( p_i \) is the estimated proportion for point \( x_i \). This method identifies the data points that are not well represented by the estimated endmembers and, thus, lie outside the convex hull defined by the endmembers.

4. EXPERIMENTAL RESULTS

Experimental evaluations have been carried out to investigate the performance of the proposed methods.

4.1 Datasets

The proposed instance influence estimation methods were tested on two hyperspectral datasets.
4.1.1 MUUFL Gulfport Data Set

The first hyperspectral data set used in experiments in this paper was acquired by the CASI-1500 hyperspectral imager over the campus of the University of Southern Mississippi-Gulfpark in Long Beach, Mississippi in November 2010. The scene contains $325 \times 337$ pixels and consists of 72 bands covering a wavelength range of 375 to 1050 nm with a 10 nm bandwidth. The spatial resolution is 1 m. Four different types of colored fabric cloths were placed throughout the scene as targets. The target colors (used to identify the different target types) are Brown, Dark Green, Faux Vineyard Green, and Pea Green. Each type of target varied in size from $0.5 \times 0.5 \text{ m}^2$, to $3 \times 3 \text{ m}^2$. A 5-by-5 halo around the center of each target was considered as the target “bag” since the accuracy of the GPS device used to collect the ground truth was 5 m.

4.1.2 Pavia University Data Set

The second data set was collected by the Reflective Optics System Imaging Spectrometer (ROSIS) around the Engineering School at the University of Pavia, Italy in July 2002. The flight was operated by the Deutschen Zentrum für Luft- und Raumfahrt (DLR, the German Aerospace Agency) in the framework of the HySens project, managed and sponsored by the European Union. The ROSIS generates 115 bands cover 430 to 860 nm with 4nm bandwidth. The scene contain $340 \times 610$ pixels and consists of 103 bands with 12 noisiest bands removed. The spatial resolution is 1.3 m. We obtained this dataset from the website of Computational Intelligence Group at the Basque University (UPV/EHU).

The target of interest for this data set was selected as a region of sidewalk (found around the blue painted metal sheets). The label of target bag and non-target bags were chosen to ensure that the target bag contains the target material and non-target bags contained a variety of non-target materials such as painted metal sheets, vegetation, red roof, bare soil and shadow.

4.2 Single Point Experiment

The first experiment investigated the correlation between the influence of a single data point and the proposed metrics. The $eFUMI$ was first run given an initial set of labels (as shown in Figure 1). When running $eFUMI$, endmembers were initialized using the VCA algorithm and all proportion values were initialized as $\frac{1}{M+1}$ where $M$ is the number of background endmembers and $M + 1$ is the total number of endmembers (given only one target endmember). After this initial run, both of the proposed methods to approximate relative influence were computed. Thus, the target proportion value and the residual error were computed for every data point. Then, the labels of 1000 non-target data points were flipped in series. For each data point, $eFUMI$ was run again given the new label set and the resulting influence value was computed. After the influence value was computed for a data point, the label of that point was restored and the next label was flipped to repeat the same process such that the influence values for all 1000 points were calculated. This process is outlined in Alg. 1.
Algorithm 1 Single Point Experiment

1: Initialize $\mathbf{E}_{init}$ via VCA, $\mathbf{P}_{init}$ as $\frac{1}{M+1}$
2: $\mathbf{E}_0, \mathbf{P}_0 \leftarrow \text{eFUMI}(L, \mathbf{X}, \mathbf{E}_{init}, \mathbf{P}_{init})$ (where $L$ is the initial label set and $\mathbf{X}$ is the data)
3: Compute residual error for each data point: $r \leftarrow \|\mathbf{X} - \mathbf{E}_0\mathbf{P}_0\|^2_2$
4: Obtain target proportion for each data point, $p_t$ via unmixing using (5)
5: for $i=1:\text{NumDataPoints}$ do
6: Flip the label $l_i$ of point $x_i$ to obtain updated label set, $L^i$: $l_i \leftarrow l_i - 1$
7: $\mathbf{E}_i, \mathbf{P}_i \leftarrow \text{eFUMI}(L^i, \mathbf{X}, \mathbf{E}_0, \mathbf{P}_0)$
8: Compute Influence: $I_i$ using (3)
9: Restore the label $l_i$: $l_i \leftarrow l_i - 1$
10: end for
11: return

Figure 2. Influence caused by selecting 1000 points randomly(a,b) or with high target proportion(c,d) from Gulfport and changing labels, compared with their corresponding (a,c) target proportion, (b,d) residual error

Figure 2 (a) and (b) display the scatter plots of log of the influence value versus the target proportion and residual error metrics, respectively, for 1000 randomly selected points. The Spearman’s rank correlation coefficients for both methods are $\rho_{pt} = 0.3875$ and $\rho_{re} = 0.1005$. Figure 2 (c) and (d) display the scatter plots of log of the influence value versus the target proportion and residual error metrics, respectively, for the 1000 data points with the largest target proportion value. The Spearman’s rank correlation coefficients for both methods are $\rho_{pt} = 0.6434$ and $\rho_{re} = 0.5674$. As can be seen in the scatter plots, points with large influence values tend to also have large target proportion and large residual error values.

The proposed methods are also shown to be effective on the Pavia University dataset. As is shown in Figure 1 (b), a sub-image of Pavia University was chosen as the test dataset. The red rectangular region was marked as the target bag and green rectangular regions were identified as the non-target bags. In this example, the target material was “sidewalk”. The labels of all non-target data points were flipped sequentially, following the procedure described above. As shown in Figure 3 (a), there is a strong relationship between high influence value and high target proportion on this data set. Figure 3 (b) displays the relationship between influence value and residual error.
and residual error. The data points that have a target proportion above 0.4 in Figure 3 (a) were identified as pixels from red roof regions in the non-target bags. Further investigation shows that these red roof materials have a similar spectral signature to the sidewalk in the area. In this way, act as a “confuser” during target characterization and, thus, they are influential data points in the eFUMI algorithm. In this example, target portion was seen to be more effective than residual error in predicting high influence values (as can been seen with the divergence of influence values in the scatter plot among points with large residual error).

4.3 Mislabeling and Recovery Experiment

In this experiment, we investigate the improvement in target endmember estimation by correcting the labels of groups of mislabeled data points. Specifically, we compare the improvement of selecting points to relabel using the proposed methods versus random selection.

The experiment was structured as follows. First, eFUMI was run with a fixed set of correct initial labels. The resulting endmembers and proportion values were labeled as $E_{\text{true}}$ and $P_{\text{true}}$. Then, 0.5% of the labels (500 non-target points) were randomly selected and changed to incorrect label values. eFUMI was run using these incorrect labels and the results were named $E_{\text{err}}$ and $P_{\text{err}}$. Finally, 20% data points were selected using one of three different strategies: (1) selected 20% of the data points randomly, (2) selected 20% of the data points with largest target proportion, and (3) selected 20% of the data points with the largest residual error. Among the 20% of selected pixels, their labels were corrected if incorrect. These updated labels were then used to run eFUMI. These final set of estimated endmembers were named $E_{\text{rand}}$, $E_{\text{pt}}$, and $E_{\text{re}}$, respectively, depending on the sample selection strategy. This process is outlined in Alg. 2.

**Algorithm 2** Mislabeling and Recovery Experiment

1: Initialize $E_{\text{init}}$ via VCA, $P_{\text{init}}$ as $\frac{1}{M+1}$
2: $E_{\text{true}}, P_{\text{true}} \leftarrow \text{eFUMI}(L, X, E_{\text{init}}, P_{\text{init}})$ (where L is the initial label set and X is the data)
3: Compute residual error for each data point: $r \leftarrow \|X - E_{0}P_{0}\|^{2}$
4: Obtain target proportion for each data point, $p_{t}$ via unmixing using (5)
5: Randomly select and flip $\alpha$% labels obtaining $L_{\text{err}}$
6: $E_{\text{err}}, P_{\text{err}} \leftarrow \text{eFUMI}(L_{\text{err}}, X, E_{\text{init}}, P_{\text{init}})$ (where L is the updated label set and X is the data)
7: Initialize $E_{0}$ via VCA, $P_{0}$ as $\frac{1}{M+1}$
8: for i=1 to 3 do
9:     if i=1 then
10:         Randomly select $\beta$% labels and correct if wrong to obtain $L_{\text{rand}}$
11:         $E_{\text{rand}}, P_{\text{rand}} \leftarrow \text{eFUMI}(L_{\text{rand}}, X, E_{0}, P_{0})$
12:         Compute DoI$_{\text{rand}}$ using (7)
13:     end if
14:     if i=2 then
15:         Select points with highest $\beta$% target proportions and correct their labels if wrong to obtain $L_{\text{pt}}$
16:         $E_{\text{pt}}, P_{\text{pt}} \leftarrow \text{eFUMI}(L_{\text{pt}}, X, E_{0}, P_{0})$
17:         Compute DoI$_{\text{pt}}$ using (7)
18:     end if
19:     if i=3 then
20:         Select points with highest $\beta$% residual errors and correct their labels if wrong to obtain $L_{\text{re}}$
21:         $E_{\text{re}}, P_{\text{re}} \leftarrow \text{eFUMI}(L_{\text{re}}, X, E_{0}, P_{0})$
22:         Compute DoI$_{\text{re}}$ using (7)
23:     end if
24: end for
25: return

Degrees of improvement (DoI) for the target endmember spectra for the three methods (random, target...
proportion and residual error) were calculated using the following:

\[
DoI_k = \frac{∥e_{ttrue} - e_{ttrue}∥^2}{∥e_{ttrue} - e_{ttrue}∥^2}, \quad k = \text{rand}, P_t, \text{re},
\]

where \(e_{tm}\) is the target endmember for \(e_m = \text{true, err, rand, P_t, re}\). DoI for the three methods were computed as \(DoI_{\text{rand}} = 18.7\%\), \(DoI_{P_t} = 96.11\%\), \(DoI_{\text{re}} = 99.42\%\), respectively, considering the brown target in the MUUFL Gulfport data set. Figure 4 and the resulting DoIs show that the label correction obtained using the proposed methods could better recover the estimated target signature as opposed to random selection.

The mislabeling and recovery experiment was repeated on the Pavia Dataset. 5% of the labels (58 non-target points) was chosen as the mislabeling ratio and 10% was chosen as the correction ratio. The initial labels for eFUMI was the same one shown in Figure 1 (b). The DoI for three methods were found to be \(DoI_{\text{rand}} = 25.26\%\), \(DoI_{P_t} = 73.4\%\), and \(DoI_{\text{re}} = 28.06\%\). Similar to the single point experiment, it was found that the target proportion metric was more effective on this data set.

### 4.4 Superpixel Influence Experiment

A superpixel is defined as a small, spatially continuous segment in an image. In this experiment, we investigate the influence of modifying labels of superpixels (as opposed to individual pixels) in a hyperspectral data set. The influence for superpixel was investigated since each superpixel generally contains data points with similar spectral signatures (and, thus, the influence of the set of data points is likely to be similar) and because it is much easier and more intuitive to relabel superpixel regions instead of individual pixels.

To understand the correlation between influence of superpixel and proposed approaches, the Gulfport dataset was over-segmented into about seven thousand superpixels having similar sizes using a Normalized Cut method. Then, the rest of experiment was very similar with single point influence experiment with one difference which is instead of computing the target proportion of all points in each superpixel, we relied on the largest target proportion in each superpixel as the surrogate influence metric. This process is outlined in Alg. 3. Figure 5 (a) shows the superpixels of Gulfport dataset. Figure 6 illustrates the plot of log of the influence value versus the log of largest target proportion, residual error, sum of target proportion, and sum of residual error in each superpixel, respectively. As is shown in Figure 6, the log of the influence is most correlated with the largest target proportion in each superpixel among all proposed estimation methods.

To further investigate superpixel influence, the same experiment was repeated on the Pavia dataset. Nearly seven hundred segments was generated and shown in 5 (b). The average size of Pavia segments is much larger than those in Gulfport. Figure 7 shows the influence value versus all of the proposed metrics for the Pavia data set. The performance of the sum of target proportions and the sum of the residual errors were found to be more effective than the maximum values. We believe this to be the case because the sizes of the superpixels on Pavia are much larger than Gulfport so that considering only one maximum point in the superpixel is not comprehensive enough as compared to metrics that take into account all target proportions or residual errors in each superpixel.
Figure 5. Influence of Superpixel for (a) Gulfport. 7419 segments were generated via Normalize Cut; (b) Pavia University. 744 segments were generated via Normalize Cut

Figure 6. Influence of Gulfport superpixels caused by flipping the labels of each superpixel compared with (a) maximum target proportion in each superpixel, (b) maximum residual error in each superpixel, (c) sum of target proportions in each superpixel, and (d) sum of residual errors in each superpixel

Algorithm 3 Superpixel Experiment

1: Segment input image into $N$ superpixels
2: Initialize $E_{\text{init}}$ via VCA, $P_{\text{init}}$ as $\frac{1}{M+1}$
3: $E_0, P_0 \leftarrow eFUMI(L, X, E_{\text{init}}, P_{\text{init}})$
4: Compute residual error for each data point: $r \leftarrow \|X - E_0 P_0\|_2^2$, compute $\max(r)$ in each superpixel, compute $\sum(r)$ in each superpixel
5: Obtain target proportion for each data point, $p_t$ via unmixing using (5), compute $\max(p_t)$ in each superpixel, compute $\sum(p_t)$ in each superpixel
6: for $i = 1:N$ do
7: Flip all of the labels for each data point in superpixel $s_i$ to obtain $L^i$
8: $E_i, P_i \leftarrow eFUMI(L^i, X, E_0, P_0)$
9: Compute Influence: $I_i$ using (3)
10: Restore the labels to $L$
11: end for
12: return
Figure 7. Influence of Pavia superpixels caused by flipping the labels of each superpixel compared with (a) maximum target proportion in each superpixel, (b) maximum residual error in each superpixel, (c) sum of target proportions in each superpixel, (d) sum of residual errors in each superpixel

5. SUMMARY

In this article, we proposed relative influence estimation metrics for the eFUMI algorithm. These provided a mechanism to estimate relative pixel and superpixel influence in eFUMI. Generally, the target proportion metric provided better performance as compared to the residual error metric.

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