Measuring evolution of a photon in an interferometer with spectrally-resolved modes

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In the year 2013, Danan et al. published a paper [Phys. Rev. Lett. 111, 240402 (2013)] demonstrating a counterintuitive behavior of photons in nested Mach-Zehnder interferometers. The authors then proposed an explanation based on the two-state vector formalism. This experiment and the authors’ explanation raised a vivid debate within the scientific community. In this paper, we contribute to the ongoing debate by presenting an alternative experimental implementation of the Danan et al. scheme. We show that no counterintuitive behavior is observed when performing direct spectrally-resolved detection.

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I. INTRODUCTION

Over the past three years, Lev Vaidman and his coworkers published several papers discussing a new method for analyzing the past of a photon detected at the output of an interferometer [1–4]. This method, based on the two-state vector formalism (TSVF), raised a vivid debate within the scientific community. In their seminal paper on this topic [4], Danan et al. presented experimental evidence for the validity of this approach. In that experiment, two nested Mach-Zehnder interferometers were constructed with mirrors A, B, C, E and F vibrating at distinct frequencies (see Fig. 1). Harmonic analysis of the output signal allowed to determine whether a photon passed by a specific mirror. Three different configurations were tested in the original experiment. In one of these configurations (labeled as “c” in the original paper) a highly counterintuitive outcome was obtained. This result was observed when the outer interferometer was disabled by blocking its lower arm (path “c”) and thus only the inner interferometer was operational. Phase shift in this inner interferometer was adjusted so that the two indistinguishable photon paths interfered destructively in the detected output port ($\phi = 0$).

Quite surprisingly, even the photons, whose paths in the interferometer had been identified by the harmonic analysis, interfered destructively. This effect seemingly violates the Englert-Greenberger-Yasin duality relation, which is related with the wave-particle duality of photons [5–10]. The authors of Ref. [4] argued that this effect can be explained by means of the TSVF. This particular experiment and the unusual interpretation of the results were subsequently followed by a number of papers [11–16]. Authors of these papers for instance provided an alternative classical formalism [11][12] for the experiment or questioned its specific implementation [13][15].

In 2015, we theoretically analyzed the Danan et al. experiment [4] and proposed a standard quantum-mechanical description of the action of vibrating mirrors introducing distinguishable modes [15]. In that paper, we also argued that the method used to process detected light in the Danan et al. experiment is not suitable because it neglects part of the signal. This is then incorrectly interpreted as observing destructive interference. In Ref. [15], we proposed a different measurement technique to reveal the path of the photon inside the interferometer. The suggested detection method is based on direct spectral power density measurement. We predicted identical results in all configurations of the Danan et al. experiment except for the counterintuitive case with blocked path “c”. Our detection method predicts quite intuitive results even in this configuration.

In this paper, we report on an experimental imple-
Our experimental setup is based on a Mach–Zehnder interferometer as depicted in Fig. 2. The interferometer consists of two polarization independent beam splitters BS$_{1,2}$ and two pentaprisms. The input light beam is generated by a modelocked femtosecond laser Mira (Coherent) with central wavelength of 826 nm, 10 nm bandwidth and the typical mean power of 1 W. The light is coupled into the interferometer through the beam splitter BS$_1$. Motorized translation stage in the lower arm is used to balance the lengths of both interferometer arms. The piezo vibration stage in the upper arm is used to change the relative phase between these arms. In this experiment, we used two identical narrow-band spectral filters F$_{1,2}$ with transmission bandwidth of 3 nm centered at 826 nm. F$_2$ was mounted on a rotation stage. By rotating the filter, we were able to shift its transmission window to shorter wavelengths. In our experiment, filters F$_1$ and F$_2$ introduce distinguishability between the interferometer arms just as the vibrating mirrors did in the original paper [4]. Finally, the beam splitter BS$_2$ couples the light from both the interferometer arms. Due to technological imperfections, BS$_1$ and BS$_2$ have not perfectly balanced splitting ratios. Also the overall transmissivity of F$_2$ depends on its rotation. Therefore, a neutral density filter (NDF) was inserted into the upper arm to balance effective losses. The Monochromator (MC) Jobin Yvon Triax 320 is located in one of the interferometer output ports and provides the capability to discriminate spectral components of the beam (shown in Fig. 2). Light was transferred from the output port of BS$_2$ to this monochromator using a single-mode fiber to maximize spatial mode indistinguishability. Detection was performed at the output of the monochromator using a Power Meter PM120 by Thorlabs (labeled D).

For the preliminary adjustments of the setup, both filters F$_{1,2}$ were rotated perpendicular to the light beam direction and the detector was placed directly to the BS$_2$ output port bypassing the monochromator. First, we ensured precise coupling of the beam to the setup. We checked, that the polarization remains unchanged while being transmitted or reflected on beam splitters. The second part of the adjustment procedure consists of several steps, which have to be repeated for each setting of the measurement. Balanced output intensities from both arms are achieved by rotating NDF wheel with gradient absorption. Then lengths of the arms were equalized by positioning the translation stage MT. Accurate setting of the MT position was adjusted by finding maximum of the autocorrelation function of the signal. We were able to reach visibility of the interferometer typically about 98 % in the initial configuration with filter F$_2$ inserted perpendicularly to the beam. The interferometer was sufficiently stable to scan the interference fringes by varying voltage on the piezo-driven translation stage.

II. EXPERIMENTAL SETUP

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FIG. 2. (color online) Experimental setup as described in the text. Individual components are labelled as follows: BS$_{1,2}$ – beam splitters, NDF – neutral-density filter, F$_{1,2}$ – narrowband filters, MT – motor translation, MC – monochromator, D – detector.
III. MEASUREMENT AND RESULTS

The purpose of our experiment is to recreate a similar situation as in the original research paper by Danan et al. [4]. But instead of using vibrating mirrors, we encode the which-path information directly into different shapes of spectra in the upper and lower interferometer arm. Further to that, our experimental configuration allows us to tune the distinguishability between the interferometer arms. This is achieved by rotation of the second filter $F_2$. In subsequent paragraphs, we label three spectral modes A, B and E in accordance to the labelling of mirrors by Danan et al. [4]. In the original experiment drawn in Fig. 1 mirrors A and B were placed in the upper and lower arm of the interferometer respectively. Mirror E stood in front of that interferometer. Observing vibration frequencies A and B thus gave information about the propagation of light in the upper and lower arm respectively. Frequency peak E did not provide any which-path information. Similarly to that, we associate spectral modes A and B with the modes maximizing the predictability of photons propagating in the upper (mode A) and lower (mode B) arm. Mode E was chosen to give least amount of predictability. In the original experiment [4], the modes with Gaussian spectral profile reflected from mirrors A and B are probabilistically distinguishable by detection of their transverse spatial modes. The beams are indistinguishable if the mirrors are deviated by equal angle from plane of the interferometer. Therefore, except particular times, the beams reflected from mirrors A and B are probabilistically distinguishable. In our experiment, the same is true for beams with quasi-Gaussian spectra shaped by filters $F_1$ and $F_2$. The probabilistic distinguishability in transversal spatial modes is intertwined with probabilistic distinguishability in spectrum.

We have performed several sets of measurements for assorted rotation angles of $F_2$. Each measurement set consists of several scans through the frequency spectrum in the range from 815 nm to 835 nm with resolution of 0.2 nm. First, we simply measured spectra separately from the upper and lower arm. We used this data to calculate theoretical predictions for the visibility. Next, for each wavelength we measured the visibility of interference as a measure of indistinguishability between the arms. The visibility is calculated from the minimal $I_{\text{min}}$ and maximal $I_{\text{max}}$ power density in an interference fringe at a given wavelength $\lambda$ using the formula

$$V(\lambda) = \frac{I_{\text{max}}(\lambda) - I_{\text{min}}(\lambda)}{I_{\text{max}}(\lambda) + I_{\text{min}}(\lambda)}.$$

(1)

The uncertainty of the power density measurement was estimated from the typical fluctuation of the power measurement of the power meter D. Typical example of one set of these spectrum scans is depicted in Fig. 3 including interference fringes at three selected wavelengths.

Based on this spectrum scan, we have selected three wavelengths corresponding to the maximum and two minima of visibility. These wavelengths are labeled E for maximum of the visibility and A, B for the two minima. Both arms contribute by equal power density at the wavelength E, thus we observe maximal interference visibility at this wavelength for the given rotation of filter $F_2$. On the other hand, frequencies A and B are chosen to maximize the distinguishability of the two respective photon paths in the interferometer.

Four representative results of the normalized power densities are summarized in Tab. 1 and visualized in Fig. 3. Black bars depict power density maxima $I_{\text{max}}$ corresponding to constructive interference, and grey bars depict power density minima $I_{\text{min}}$ corresponding to destructive interference. To obtain normalized values of $I_{\text{max}}$ and $I_{\text{min}}$, we have divided the measured spectral power densities by four times the spectral power density measured separately with one arm blocked. The factor 4 arises from the fact that only one quarter of the signal entering the interferometer leaves by the detected output port if one arm is blocked. As it is evident from the experimental setup shown in Fig. 2, the signal is divided in half on each of the two balanced beam splitters. Inner red bars depict theoretical predictions calculated using the formulas for perfect constructive and destructive in-

![FIG. 3. (color online) Example of measured data for $F_2$ rotated by 14 deg. resulting in $\Delta \lambda = 4.9$ nm. Triangles and squares represent independent spectral power density for lower and upper arms. Circles visualize obtained visibility. Vertical lines labelled A, E and B mark the selected wavelengths corresponding to maximum and two minima of the visibility. Interference fringes (spectral power density as function of mutual phase shift between interferometer arms) are visualized for the selected modes A, B and E.](image-url)
TABLE I. Measured minimum and maximum normalized power densities in an interference fringe for various rotations of the filter F2. Theoretical prediction shown below is based on individual spectra taken from the interferometer arms separately.

| Δλ   | Frequency mode A | Frequency mode B | Frequency mode E |
|------|------------------|------------------|------------------|
|      | \( I_{\text{max}} \) | \( I_{\text{min}} \) | \( I_{\text{max}} \) | \( I_{\text{min}} \) |
| 1.4 nm | 0.519 ± 0.005 | 0.089 ± 0.002 | 0.555 ± 0.007 | 0.094 ± 0.003 | 0.902 ± 0.006 | 0.014 ± 0.001 |
| 2.4 nm | 0.388 ± 0.006 | 0.171 ± 0.004 | 0.398 ± 0.005 | 0.140 ± 0.003 | 0.868 ± 0.006 | 0.020 ± 0.001 |
| 4.9 nm | 0.309 ± 0.007 | 0.240 ± 0.006 | 0.318 ± 0.005 | 0.190 ± 0.003 | 0.958 ± 0.020 | 0.028 ± 0.005 |
| 6.5 nm | 0.274 ± 0.005 | 0.234 ± 0.005 | 0.300 ± 0.006 | 0.214 ± 0.005 | 0.925 ± 0.030 | 0.039 ± 0.010 |

FIG. 4. (color online) Processed measurement data for four rotations of F2, which correspond to spectral distance Δλ = 1.4, 2.4, 4.9 and 6.5 nm. Black bars represent normalized maximum spectral power densities (constructive interference) for wavelengths A, B, and E. Grey bars, in a similar way, represent spectral power density minima (destructive interference). Theoretical predictions are shown using the inner red bars.

As a next step, we have subjected the obtained data to the Englert-Greenberger-Yasin inequality test [5, 9] expressed in the form of

\[
V^2(\lambda) + D^2(\lambda) \leq 1,
\]

where \( V(\lambda) \) stands for visibility and \( D(\lambda) \) for distinguishability of the paths given by absolute value of the difference between normalized power densities from the first (\( I_1 \)) and from the second arm (\( I_2 \))

\[
D(\lambda) = \left| \frac{I_1(\lambda) - I_2(\lambda)}{I_1(\lambda) + I_2(\lambda)} \right|.
\]

By using this test, we can verify the consistency of our measurements with standard quantum-mechanical limits. Our results are summarized in Table I. Note, that in the case of the original experiment by Danan et al., the inequality \( (3) \) is seemingly violated, because the frequency modes A and B allegedly interfere with high visibility despite the fact, that they provide exact which-path information (\( D \to 1 \)).

Our obtained results show that, quite intuitively, the visibility decreases as the frequency modes A and B become more distinguishable (higher rotation angles of filter F2). For perfectly distinguishable modes, visibility should drop to zero. As a result, the signal at wavelengths corresponding to frequency modes A and B is nearly constant independent of the setting of the mutual phase shift between the interferometer arms.

We observe almost perfect distinguishability when rotating the filter F2 to achieve spectral distance Δλ = 6.5 nm (more than twice full width at half maximum of the relevant peaks). In this case, the situation is analogous to the experiment by Danan et al. with the outer interferometer blocked (see Fig. 1). Even when setting destructive interference to occur in the detected output port, the probability of observing photons at frequencies either A or B are nonzero [see grey bars in Fig. 4 (Δλ = 6.5 nm)]. On the other hand, the probability of observing photons with frequency E vanishes. Measured probabilities of observing photons at frequencies A, B and E are reaching values 0.234±0.005, 0.214±0.005 and 0.039±0.010, respectively. Our theoretical model predicts the values to be 0.25, 0.25 and 0 respectively [15]. We attribute these small discrepancies to non-perfect distinguishability of the two modes A and B and imperfect interference at frequency E.

IV. HARMONIC ANALYSIS METHOD

Let us now focus on the differences and similarities between our experiment and the measurements performed.
TABLE II. Measured values of visibility $V$ and distinguishability $D$ for various setting of the filter $F_2$ rotation.

| $\Delta \lambda$ (nm) | Frequency mode A | Frequency mode B | Frequency mode E |
|-----------------------|------------------|------------------|------------------|
|                       | $V$              | $D$              | $V^2 + D^2$      | $V$              | $D$              | $V^2 + D^2$      |
| 1.4                   | 0.71 $\pm$ 0.01  | 0.66 $\pm$ 0.01  | 0.94 $\pm$ 0.02  | 0.71 $\pm$ 0.01  | 0.64 $\pm$ 0.02  | 0.91 $\pm$ 0.02  | 0.97 $\pm$ 0.01  | 0.96 $\pm$ 0.01  | 0.94 $\pm$ 0.01  |
| 2.4                   | 0.39 $\pm$ 0.01  | 0.92 $\pm$ 0.02  | 1.00 $\pm$ 0.04  | 0.48 $\pm$ 0.01  | 0.85 $\pm$ 0.02  | 0.95 $\pm$ 0.03  | 0.95 $\pm$ 0.01  | 1.11 $\pm$ 0.01  | 0.93 $\pm$ 0.01  |
| 4.9                   | 0.13 $\pm$ 0.01  | 0.99 $\pm$ 0.03  | 1.00 $\pm$ 0.05  | 0.23 $\pm$ 0.01  | 0.97 $\pm$ 0.02  | 1.00 $\pm$ 0.04  | 0.94 $\pm$ 0.01  | 0.04 $\pm$ 0.01  | 0.89 $\pm$ 0.01  |
| 6.5                   | 0.08 $\pm$ 0.01  | 0.99 $\pm$ 0.02  | 0.99 $\pm$ 0.05  | 0.17 $\pm$ 0.01  | 0.98 $\pm$ 0.02  | 0.99 $\pm$ 0.05  | 0.92 $\pm$ 0.01  | 0.01 $\pm$ 0.02  | 0.85 $\pm$ 0.01  |

FIG. 5. (color online) Spectral dependency of normalized power of minima of interference fringe for $\Delta \lambda = 4.9$ nm. Schematically are depicted two parts of detector centered at frequency $\lambda_s$ (spectral mode E). $P^+$ and $P^-$ denote normalized intensities in their respective bins.

by Danan et al. in Ref. [4]. They used vibrating mirrors to deflect the beam which left a weak mark on its direction. This weak deviation was then inspected using a quad-cell detector measuring difference of the photocurrents generated in the both halves of the detector. In our experiment, we used tunable spectral narrow-band filters to leave a which-path mark on the propagating photons instead.

For every selected wavelength, we measured an interference fringe. The maximal and minimal power intensities ($I_{\text{max}}(\lambda)$ and $I_{\text{min}}(\lambda)$) were used to calculate the visibility. The minima of the normalized power interference fringes are plotted in Fig. 5. The interferometer was set for destructive interference ($\varphi = 0$).

Here the monochromator is formally equivalent to the quad-cell detector distinguishing the above-mentioned marks. While the quad-cell detector registers intensity fluctuations of the resulting interference pattern due to the beam sweeping across its halves, the monochromator distinguishes the spectral marks directly. We emulate the sweep by accumulating the spectra for various rotations of filter $F_2$. Similar to the halves of the quad-cell detector, we have divided the obtained spectra into two bins (see Fig. 5). This division between the bins was made at the wavelength $\lambda_s$ associated with the mode E. This mode corresponds to maximum indistinguishability like the central axis of the quad-cell detector. In Fig. 6 we summarize normalized powers integrated over the two selected bins

$$P^+ = \int_{0}^{\Delta \lambda} I_{\text{min}}(\lambda) d\lambda / \int_{0}^{\Delta \lambda} I_{\text{max}}(\lambda) d\lambda,$$

$$P^- = \int_{\Delta \lambda}^{\infty} I_{\text{min}}(\lambda) d\lambda / \int_{\Delta \lambda}^{\infty} I_{\text{max}}(\lambda) d\lambda,$$

and their difference $\Delta P = P^+ - P^-$. For large spectral overlap of the filters $F_1$ and $F_2$, the interference fringe is deeply modulated and the integrated minimal intensities $P^+$ and $P^-$ are small. Increasing the spectral distance of the filters $\Delta \lambda$, the interference visibility decreases leading to higher values of binned intensities $P^+$ and $P^-$. Simultaneously the predictability of the photon path increases. But even though there is clearly a distinguishable signal from the two arms of the interferometer, $\Delta P$ simply ignores the which-path information due to the subtraction of $P^+$ and $P^-$. It does not act as a reliable which-path witness. In our experiment, the mean value of $\Delta P = 0.020 \pm 0.03$ is about one order of magnitude smaller than mean values of $P^+ = 0.134 \pm 0.002$ and $P^- = 0.122 \pm 0.002$. Ideally $\Delta P$ should be zero. This is mathematically similar to the Danan et al. experiment, where they measured difference of the photocurrents generated in the two halves.
of the quad-cell detector. Due to the symmetry of the light profile on the detector the which-path information was lost.

V. CONCLUSIONS

In this paper, we have demonstrated an alternative which-path detection method to the original harmonic analysis used in Ref. [4]. Our method is based on direct frequency resolution of the signal at the output of the interferometer. In contrast to the harmonic analysis, our method yields quite intuitive results that do not violate the Englert-Greenberger-Yasin inequality. We have shown that when the frequency modes corresponding to respective arms of the interferometer are completely distinguishable, the interference vanishes and signal is observed independently on mutual phase shift between the interferometer arms. On the other hand, frequency modes that give no which-path information manifest high interference visibility as expected.

We have also implemented detection method analogous to the one used in the Danan et al. experiment [4]. Our analysis demonstrates how the which-path information gets lost in this process. This supports our original finding [15], that in the Danan et al. experiment [4], the missing signal at frequencies A and B was caused by unsuitable detection method rather then by an interference effect. We hope that these results would further contribute to the ongoing scientific debate which follows the exciting experiment by Danan et al. from 2013.

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