ARE THERE MACH CONES IN HEAVY ION COLLISIONS?
THREE-PARTICLE CORRELATIONS FROM STAR

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We present results from STAR on 3-particle azimuthal correlations for a 3 < p_T < 4 GeV/c trigger particle with two softer 1 < p_T < 2 GeV/c particles. Results are shown for pp, d+Au and high statistics Au+Au collisions at √s_NN = 200GeV. We observe a 3-particle correlation in central Au+Au collisions which may indicate the presence of conical emission. In addition, the dependence of the observed signal angular position on the p_T of the associated particles can be used to distinguish conical flow from simple QCD-ˇCerenkov radiation. An important aspect of the analysis is the subtraction of combinatorial backgrounds. Systematic uncertainties due to this subtraction and the flow harmonics v_2 and v_4 are investigated in detail.

1. Introduction

Heavy ion collisions create a medium that may be the quark gluon plasma (QGP). This medium can be studied through jets and jet-correlations. Jets make a good probe because their properties can be calculated in the vacuum with perturbative quantum chromodynamics (pQCD). Two-particle jet-like azimuthal correlations have shown the away-side shape in central Au+Au collisions to be broadened with respect to pp and peripheral Au+Au collisions or even double humped (see Fig. 1a). The away-side structure is consistent with many different physics mechanisms including: large angle gluon radiation, jets deflected by radial flow or preferential selection of particles due to path-length dependent energy loss, hydrodynamic conical flow generated by Mach-cone shock waves, and Čerenkov radiation. Three-particle correlations can be used to differentiate conical flow and Čerenkov radiation, which have the characteristic of conical emission, from other mechanisms. In addition, the associated particle p_T dependence of the conical emission angle can be used to differentiate between hydrodynamic conical flow and simple Čerenkov radiation.
2. Analysis Procedure

The 3-particle correlation analysis method is rigorously described in 9. The results reported here are for charged trigger particles of $3 < p_T < 4$ GeV/c and two charged associated particles of $1 < p_T < 2$ GeV/c (except where otherwise noted). The data were all taken in the STAR time projection chamber for $pp$, $d+Au$ and $Au+Au$ collisions at $\sqrt{s_{NN}}=200$ GeV/c.

Figure 1 shows the raw 3-particle azimuthal distribution in $\Delta \phi_{aT} = \phi_a - \phi_T$ and $\Delta \phi_{bT} = \phi_b - \phi_T$ where $\phi_T$, $\phi_a$, and $\phi_b$ are the azimuthal angles of the trigger particle and the two associated particles respectively. Combinatorial backgrounds must be removed to obtain the genuine 3-particle correlation signal. The analysis is performed by treating the events as composed of two components, particles that are jet-like correlated with the trigger particle and background particles. One source of background, the hard-soft background, results when one of the associated particles has a jet-like correlation with the trigger particle and the other is uncorrelated, except for the correlation due to flow. The background is constructed from the 2-particle jet-like correlation, $\hat{J}^2_{2}$, folded with the normalized 2-particle background, $B^{inc2}$, Fig. 1a. The 2-particle background is constructed by mixing events with the flow modulation added in pairwise from the average $v_2$ values from the measurements based on the reaction plane and 4-particle cumulant methods 1. For the $v_4$ contribution we use the parameterization $v_4 = 1.15 v_2^2$ from the data 10. The background is normalized (with scale factor $\alpha$) to the signal within $0 < |\Delta \phi| < 1.2$ (zero yield at 1 radian or ZYA1). We shall refer to the hard-soft background as $\hat{J}_2 \otimes \alpha B^{inc2}$.

Another source of background, the soft-soft background, results from correlations between the two associated particles which are independent of the trigger particle. This background is obtained from mixed events, where the trigger particle and the associated particles are from different events in the same centrality window. We shall refer to the soft-soft background as $B^{inc3}$. Since the two associated
ARE THERE MACH CONES IN HEAVY ION COLLISIONS? THREE-PARTICLE CORRELATIONS FROM STAR

particles are from the same event, this background contains all of the correlations between the two associated particles that are independent of the trigger particle, including correlations from minijets, other jets in the event, and flow.

The flow between the two associated particles that is independent of the trigger particle was accounted for in the soft-soft term, but particles are also correlated with the trigger particle via flow. The trigger flow is added in triplet-wise from mixed events, where the trigger and associated particles are all from different events in the same centrality window. The \( v_2 \) and \( v_4 \) values are obtained the same way as for the 2-particle background. The number of triplets is determined from the inclusive events. We shall refer to the backgrounds from trigger flow as \( B_{inc,TF}^3 \). The total background is then, \( \hat{J}_2 \otimes \alpha B_2^{inc} + \beta \alpha^2 (B_3^{inc} + B_3^{inc,TF}) \). Both \( B_3^{inc} \) and \( B_3^{inc,tf} \) are scaled by \( \beta \alpha^2 \). The normalization \( \alpha^2 \) corrects for the multiplicity bias from requiring a trigger particle. The factor \( \beta \) accounts for the effect of non-poisson multiplicity distributions and is obtained such that the number of associated pairs in the background subtracted jet-like three-particle correlation signal equals the square of the number of associated particles in the background subtracted jet-like two-particle correlation signal. Figure 1c and d show \( \beta \alpha^2 B_3^{inc} \) and \( \hat{J}_2 \otimes \alpha B_2^{inc} + \beta \alpha^2 B_3^{inc,TF} \), respectively.

3. Results

![Figure 2](image_url)

Figure 2 shows background subtracted 3-particle jet-like correlation signals. The \( pp \) and \( d+Au \) results are similar. Peaks are clearly visible for the near-side, \((0,0)\), the
Jason Glyndwr Ulery For the STAR Collaboration

away-side, \((\pi, \pi)\) and the two cases of one particle on the near-side and the other on the away-side, \((0, \pi)\) and \((\pi, 0)\). The away-side peak displays diagonal elongation that is consistent with \(k_T\) broadening. The peripheral Au+Au results show additional on-diagonal elongation of the away-side peak which may be due to contribution from deflected jets. The additional on-diagonal broadening persists into the more central Au+Au collisions. In addition, the more central Au+Au collisions display an off-diagonal structure, at about \(\pi \pm 1.45\) radians, that is consistent with conical emission. The structure increases in magnitude with centrality and is prominent in the high statistics top 12% central data provided by the on-line ZDC trigger.

![Graphical representation of the centrality dependence of the average signal strengths in different regions.](image)

**Fig. 3.** (color online) (left) Average signals in 0.7 x 0.7 boxes at \((0,0)\) (triangle), \((\pi,\pi)\) (star), \((\pi \pm 1.45,\pi \pm 1.45)\) (square), and \((\pi \pm 1.45,\pi \mp 1.45)\) (circle). (right) Differences in average signals, between \((\pi \pm 1.45,\pi \pm 1.45)\) and \((\pi \pm 1.45,\pi \mp 1.45)\) (triangle), between \((\pi \pm 1.3,\pi \pm 1.3)\) and \((\pi \pm 1.3,\pi \pm 1.3)\) (square), and between \((\pi \pm 1.0,\pi \pm 1.0)\) and \((\pi \pm 1.0,\pi \pm 1.0)\) (circle). Solid error bars are statistical and shaded are systematic. \(N_{\text{part}}\) is the number of participants. The ZDC 0-12% points (open symbols) are shifted to the left for clarity.

Figure 3 (left) shows the centrality dependence of the average signal strengths in different regions. The off-diagonal signals (circle) increase with centrality and significantly deviate from zero in central Au+Au collisions. The locations of the off-diagonal signals were determined from a double Gaussian fit to a strip projected to the off-diagonal, Fig. 4, and were found to be 1.45 radians from \(\pi\). The differences between on-diagonal signals, where both conical emission and deflected jets may contribute, and off-diagonal signals, where only conical emission contributes is shown in figure 3 (right). Since conical emission signals are expected to be of equal magnitude on-diagonal as off-diagonal, the difference may indicate the contribution from deflected jets. The difference decreases with distance from \((\pi, \pi)\).

The Mach cone emission angle is expected to be independent of the associated particle momentum, while the Čerenkov radiation model in Ref. 7 predicts an emission angle that is sharply decreasing with increasing associated particle momentum. Figure 5 (left) shows the dependence the off-diagonal peak angle on associated particle \(p_T\). The angle is consistent with constant as a function of associated particle \(p_T\).

Figure 5 (right) shows the centrality dependence the off-diagonal peak angle.
ARE THERE MACH CONES IN HEAVY ION COLLISIONS? THREE-PARTICLE CORRELATIONS FROM STAR

Fig. 4. (color online) Away-side projections of a strip of width 0.7 radians for (left) d+Au and (right) 0-12% ZDC Triggered Au+Au. Off-diagonal projection (solid) is \((\Delta \phi_1 - \Delta \phi)/2\) and on-diagonal projection (open) is \((\Delta \phi_1 + \Delta \phi)/2 - \pi\). Shaded bands are systematic errors.

Fig. 5. (color online) Emission angles from double Gaussian fits. (left) Angle as a function of associated particle \(p_T\) for Au+Au 0-12% ZDC triggered data (filled) and Au+Au 0-50% from minimum bias data (open). (right) Angle as a function of centrality for Au+Au 0-12% ZDC triggered data (circle) and Au+Au 30-50%, 10-30% and 0-10% from minimum bias data (square). The 0-12% point has been shifted for clarity. Corresponding off-diagonal peak values from fits to a constant are indicated in the legends. The dashed line is at \(\pi/2\). Solid error bars are statistical and shaded are systematic.

The angle is consistent with remaining constant as a function of centrality for mid-central and central Au+Au collisions. The solid line at 1.46 on the plot is from a fit to a constant.

4. Systematics

The major sources of systematic error are the elliptic flow measurement and the normalization. The default \(v_2\) used is the average those measured by the reaction plane and 4-particle cumulant methods. We use the reaction plane and 4-particle cumulant \(v_2\) as the upper and lower bounds to estimate the systematic uncertainty of the \(v_2\) subtraction. Figure 6a and b show the background subtracted 3-particle correlation for reaction plane and 4-particle \(v_2\) respectively. The signal is robust with respect to this variation. The hard-soft background and trigger flow backgrounds individually vary a great deal with the change in elliptic flow but the variations cancel to first order in the sum.
To study the effect of the normalization the size of the normalization window was doubled to $0.6 < |\Delta \phi| < 1.4$. The signal is robust with respect to this change in normalization. Other sources of systematic error include the effect on the trigger particle flow from requiring a correlated particle ($20\%$ on trigger particle $v_2$), uncertainty in the $v_4$ parameterization, and multiplicity bias effects on the soft-soft background. The systematic errors shown in figures include all sources mentioned.

5. Conclusion

Three-particle azimuthal correlations have been studied for trigger particles of $3 < p_T < 4 \text{ GeV/c}$ and associated particles of $1 < p_T < 2 \text{ GeV/c}$ in $pp$, $d+Au$, and $Au+Au$ collisions at $\sqrt{s_{NN}}=200 \text{ GeV/c}$ by STAR. This analysis treats events as the sum of two components, particles that are jet-like correlated with the trigger and background particles. On-diagonal broadening has been observed in $pp$ and $d+Au$ consistent with $k_T$ broadening. Additional on-diagonal broadening has been seen in $Au+Au$ collisions possibly due to deflected jets. Off-diagonal peaks consistent with conical emission are present in central $Au+Au$ collisions. To discriminate between Mach cone emission and simple Čerenkov gluon radiation, a study of the associated particle $p_T$ dependence was performed. No strong $p_T$ dependence of the angles on associated particle $p_T$ is observed. This result is consistent with Mach cone emission.

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