Fisheye lens design for solar-powered mobile ultrasound devices

Seonho Ryu\textsuperscript{a}, Jaemyung Ryu\textsuperscript{a,*} and Hojong Choi\textsuperscript{b,*}
\textsuperscript{a}Department of Optical System Engineering, Kumoh National Institute of Technology, Gumi, Korea
\textsuperscript{b}Department of Electronic Engineering, Gachon University, Seongnam, Korea

Abstract.
BACKGROUND: Compared to benchtop ultrasound machines, mobile ultrasound machines require portable batteries when acquiring information regarding human tissues during outdoor activities.
OBJECTIVE: A novel fisheye lens type was designed to address the charging issue where it is difficult to constantly track the sun. This method does not require the use of a mechanical motor that constantly tracks the sun to charge the portable batteries.
METHODS: To obtain an optical solar power system, the numerical aperture (NA) and field angle must be increased. Therefore, we use the fisheye lens with the largest field angle.
RESULTS: The NA of the designed fisheye lens system reaches 0.75, allowing light collection of approximately $\pm 48^\circ$. Additionally, the efficiency ratio of the central and surrounding areas also satisfies more than 80% at a field angle of 85$^\circ$ and more than 70% at field angles of 85$^\circ$ to 90$^\circ$, respectively.
CONCLUSIONS: We designed a novel fisheye lens for solar-powered mobile ultrasound machines used outdoors.

Keywords: Mobile ultrasound machines, fisheye lens, solar power

1. Introduction

Ultrasound machines are typically used to check the conditions of patients or cracks in steel for non-destructive testing or applying acoustic power for clinical or surgical purposes [1,2]. Compared with computed X-ray, tomography, positron emission tomography, and magnetic resonant imaging, ultrasound machines are relatively inexpensive imaging modalities [2–5]. Currently, mobile ultrasound machines are widely used for emergency rooms in hospitals or outdoor activities such as sports owing to advanced semiconductor technologies [6–9]. Mobile ultrasound machines with battery modules can be utilized without any power cords and can remotely send the imaging data using communication channels [10–12]. The received imaging data can be checked by clinical specialist for immediate diagnosis. This could be very useful for emergency cases or prevention of side effects [13]. Compared with benchtop ultrasound machines used in clinics or hospitals, mobile ultrasound machines are suitable for outdoor activity owing to portable batteries [14,15]. Because of their limited battery lives, mobile ultrasound machines should be charged in advance for emergency cases during application in high altitude regions such as
Fig. 1. Conceptual block diagram of (a) mobile ultrasound machines attached to or separated from the solar-powered panels and (b) designed fisheye lens optical system for mobile ultrasound machines.

mountains [16]. Therefore, mobile ultrasound companies provide solar-power panels attached behind the machines or solar-panel devices separated from the ultrasound machines [17,18].

Solar-powered panels utilize mechanical motors requiring additional power for the reflectors [19]. The mechanical motors generate noise that cannot be removed during image processing for patient images [20,21]. Therefore, the unwanted noise signals directly affect the imaging quality of the mobile ultrasound machines [22–25]. Additionally, mobile ultrasound machines have lower image quality than the benchtop ones because of the reduced number of ultrasound probe channels partially caused by the portable batteries [26–29]. This is because ultrasound companies should consider the available transducer channels because of excessive heat [30–32]. To replace the mechanical motors that track the sun to charge the batteries, a fisheye lens was designed to receive sunlight efficiently. A reflector-tracking system was used to track the sun in the solar power generation [23]. However, a mechanical motor is required to rotate the reflector thus electricity is consumed to drive the motor. To constantly receive sunlight without the reflector, we designed a fisheye optical lens which requires a large NA. Figure 1(a) shows the block diagram of two typical types of mobile ultrasound machines attached to or separated from solar-powered panels. Figure 1(b) shows the designed fisheye lens. As shown in Fig. 1(b), the fisheye lens modules are designed to receive sunlight without the reflector. In the optical system, the converter is designed with a spherical lens, and the aspherical surface for relay optics can be applied to an inexpensive material for automobile head lamps.

2. Methods

The optical system used for the mobile ultrasound machine proposed in this study should have a high NA. To generate power for an extended period of time, light must be received regardless of the altitude of the sun; therefore, the field angle of the optical system must be wide [33–36]. A fisheye lens with a very wide field angle and high NA should be designed to achieve this [37]. To design an optical system that satisfies the given specifications, a converter system capable of converting the field angle is designed. Here, optical systems with a typical field angle which are coupled behind the stop are referred to as relay optics. Therefore, the converter system must be positioned in front of the stop, and the distance between the two optical systems must be adjusted so that the exit pupil of the converter and entrance pupil of the relay optics to be combined are matched. Particularly, the converter in front of the stop converts light with a half field angle of 90° into a small field incident angle, and the relay optics behind the stop are designed and combined to have a high NA. When combining two optics, the angle of the chief ray passing through the converter and entering the stop should match the field angle of the relay optics [38]. Figure 2 shows
the paraxial layout of a converter in which lenses with negative and positive refractive power values are combined [39]. Therefore, the refractive power of the optical converter should be zero, and the angle of the chief ray decreases from $\theta$ to $\theta_2$.

In Fig. 2, $n_0$, $n_1$, and $n_2$ represent the refractive indices at the object plane, between the two lenses, and at the stop, respectively. Considering that the optical system is used in air, these values are all equal to 1. The distance between the two lenses is $d_1$, and the refractive power values of the two lenses are $k_1$ and $k_2$, respectively. Therefore, the refractive power of this system is given by Eq. (1). Simultaneously, the chief ray is incident on $\theta_0$, and the height of the first surface is $h_1$ that is, $u_0 = \tan \theta_2$. When the chief ray passes through the first lens, the refraction angle $u_1$ is calculated using the refraction equation shown in Eq. (2). After refraction from the first lens, the height $h_2$ is expressed as Eq. (3) if the chief ray travels by $d_1$. Further, the chief ray is refracted by the second lens, resulting in $u_2$ as shown in Eq. (4). Here, the angle of the chief ray passing through the optical system is $\theta_2$ that is, $u_2 = \tan \theta_2$. Equation (4) is the conversion equation of the light rays passing through the converter lens by substituting Eqs (2) and (3). Because the angular magnification can be defined as the ratio of the incident and exit angles of the chief ray, it can be expressed as Eq. (5), and can be obtained by substituting Eqs (1) and (4) into Eq. (5). Substituting Eq. (5) into Eq. (1) again, the refractive power of each lens constituting the converter lens can be calculated as in Eq. (6). Therefore, as shown in Eq. (6), the refractive power for each lens of the converter is determined by the angular magnification $m$ and distance $d_1$ between the lenses [40,41].

$$K = k_1 + k_2 - \frac{d_1}{n_1}k_1k_2 = 0 = \frac{1}{EFL}$$  \hfill (1)

$$h_2 = h_1 + d_1u_1$$  \hfill (2)

$$n_1u_1 = n_0u_0 - h_1k_1$$  \hfill (3)

$$n_2u_2 = n_1u_1 - h_2k_2 = n_0u_0 \left(1 - k_2 \frac{d_1}{n_1}\right) - h_1K$$  \hfill (4)

$$m = \frac{n_2u_2}{n_0u_0} = \frac{n_2 \tan \theta_2}{n_0 \tan \theta_0} = 1 - k_2 \frac{d_1}{n_1} = - \frac{k_2}{k_1} (\because K = 0)$$  \hfill (5)

$$\therefore k_1 = \frac{m - 1}{d \cdot m} \quad k_2 = - \frac{m - 1}{d}$$  \hfill (6)

The refractive power of the two lenses of the optical system shown in Fig. 2 can be calculated by Eq. (6). Therefore, the angular magnification $m$ is determined by the angle to be converted in the optical system, and the refractive power of the two lenses can be obtained if the distance $d_1$ between the two
lenses is properly determined. Substituting \( m = 0.6 \) and \( d_1 = 2.0 \) mm into Eq. (6), \( k_1 \) and \( k_2 \) become 0.333 mm\(^{-1}\) and \( k_1 = +0.200 \) mm\(^{-1}\), respectively. The converter and singlet calculated using this method are combined, and the result is shown in Fig. 3(a). Here, the singlet was designed by the method mentioned in [42–44]. In the optical system shown in Fig. 3(a), a lens was added because the field angle does not satisfy 90°. Because chromatic aberration may occur in the singlet corresponding to the relay optics, the singlet was divided and converted into an air-spaced doublet. This way, the equivalent lens method was used to divide the singlet into a doublet [45]. The layout of the optical system in which this method is applied is shown in Fig. 3(b). The paraxial design (Fig. 3(b)) does not satisfy sufficient optical performance. To increase the power generation, the entrance pupil diameter (EPD) of the optical system as shown in Fig. 3(b) must be increased. A large EPD indicates a large NA. Therefore, it is necessary to proceed with the optical design so that the NA is increased and the spot size on the image surface is minimized.

3. Results and discussion

Figure 4 shows the layout of the optical system that satisfies the optical performance. For this optical system, the effective field length (EFL) is 0.885 mm, NA is 0.750, and the overall length of the optical system is approximately 16.1 mm. The light is collected in a solar cell with the optical system as shown.
in Fig. 4. Therefore, several such modules can be installed if the amount of power generated by one solar cell is not sufficient.

Figure 5(a) shows the spot diagram in the optical system where the optical design is completed as shown in Fig. 4. The spot diagram refers to the distribution of the ray bundle passing through the optical system for each field angle. The minimum size of the solar panel cell is determined from the height of the chief ray and spot size. The height of the chief ray is 1.49 mm as shown in Fig. 4, and it can be observed that the spot size is approximately 0.14 to 0.21 mm as shown in Fig. 5(b). Therefore, the cell size is determined by the sum of the height of the chief ray and spot size. Because the field angle in which light is incident is $\pm 90^\circ$, the size of the solar cell must be $3.42 \times 3.42$ mm or more. Power generation is possible for our designed optical system regardless of the incident angle of the sunlight.

To compare the power generation produced by this optical system over time, we presented the result shown in Fig. 5(b) which is a power graph based on the field angle. The ratio of the power generation at the center and periphery is more than 80% at approximately $80^\circ$ and more than 70% at $90^\circ$. This indicates that the ratio of the minimum generation in the morning and afternoon compared to noon is more than 70%. There is a difference in the amount of light between noon sunrise or sunset; therefore, the actual power generation over time is expected to be lower than the obtained results. However, because the FOV is $\pm 90^\circ$, power generation is possible without moving the panel or optical system in the direction of the light. If the array is configured as shown in Fig. 1, light with a field angle of $\pm 90^\circ$ may not be incident on the solar cell. When configured as an array, the field angle incident on the solar cell is about $\pm 74.341^\circ$ as shown in Fig. 4. If it is located around the array, light of $\pm 90^\circ$ is incident. Thus, the optical design was performed based on the field angle of $\pm 90^\circ$.

A novel fisheye lens type was designed to overcome the charging problem of constantly tracking the sun. With these optics, it is not necessary to use a mechanical motorized power generation system to track the altitude of the existing sun.

4. Conclusion

Conventional systems used for solar power generation use parabolic mirrors. The parabolic mirror has a very small field angle and can only be used at a specific time. To overcome this, the parabolic mirror must be applied alongside a mechanical motor to track the sun. However, a system with a mechanical
motor uses some of the energy generated to drive the mechanical motor. Therefore, a fisheye lens that can receive light from all field angles was used to solve this problem. To increase the amount of power generation, the entrance pupil of the fisheye lens must be increased. The optical system must have a high NA to achieve this. An optical system that satisfies these requirements was designed by separating the converter to change the field angle and relay optics to collect light at a spot.

The converter located in front of the aperture is designed so that the incident angle on the aperture is similar to that of the relay optics. However, if a converter is simply used, the field angle does not satisfy 90°, thus a lens is added. Additionally an air-spaced doublet was configured to correct the chromatic aberration of relay optics and increase the NA. For comparison, the amount of power produced by the designed optical system over time was estimated. From the results, the relative illumination of the optical system was 80% or more up to a field angle of 80°. Therefore, the power generation ratio will be 80% when the field angle is 0° and 80°. Therefore, solar power generation is possible at any time, and it is expected that mobile ultrasonic devices can be more effective using our designed fish-eye system.

In cloudy weather, electricity may not be sufficient. However, this problem occurs not only in the system, but also in all solar power systems. In the system of this study, the solar cell and the optical system are integrated. Therefore, it is expected that the amount of power generation can be increased by combining them in an array form.

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Conflict of interest

None to report.

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