Constraining Supersymmetry using the relic density and the Higgs boson

Sophie Henrot-Versilé, Rémi Lafaye, Tilman Plehn, Michael Rauch, Dirk Zerwas, Stéphane Plaszczyński, Benjamin Rouillé d’Orfeuil, Marta Spinelli

1LAL, CNRS/IN2P3, Orsay Cedex, France
2LAPP, Université de Savoie, IN2P3/CNRS, Annecy, France
3Institut für Theoretische Physik, Universität Heidelberg, Germany
4Institute for Theoretical Physics, Karlsruhe Institute of Technology (KIT), Karlsruhe, Germany

Recent measurements by Planck, LHC experiments, and Xenon100 have significant impact on supersymmetric models and their parameters. We first illustrate the constraints in the mSUGRA plane and then perform a detailed analysis of the general MSSM with 13 free parameters. Using SFitter, Bayesian and Profile Likelihood approaches are applied and their results compared. The allowed structures in the parameter spaces are largely defined by different mechanisms of dark matter annihilation in combination with the light Higgs mass prediction. In mSUGRA the pseudoscalar Higgs funnel and stau co-annihilation processes are still avoiding experimental pressure. In the MSSM stau co-annihilation, the light Higgs funnel, a mixed bino–higgsino region including the heavy Higgs funnel, and a large higgsino region predict the correct relic density. Volume effects and changes in the model parameters impact the extracted mSUGRA and MSSM parameter regions in the Bayesian analysis.

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I. INTRODUCTION

When trying to understand the physics of the electroweak scale we encounter a set of experimental and theoretical problems. First, the discovery of a narrow, most likely fundamental Higgs scalar means that the hierarchy problem is now real \cite{1}. Second, dark matter search experiments like Xenon100 are starting to cut into the available parameter space of a weakly interacting dark matter particle \cite{2}. Third, in the 7 TeV and 8 TeV runs there seems to be no hint for any physics beyond the Standard Model at ATLAS, CMS, and LHCb.

On the other hand, the particle nature of dark matter is the most attractive hypothesis. The key observable in such models is the current dark matter density in the Universe. The Planck collaboration has recently released their data on the cosmological microwave background temperature anisotropies \cite{3}. In the ΛCDM scenario they determine the dark matter density $\Omega_{cdm} h^2$ with an unprecedented accuracy \cite{4}.

Even in supersymmetric models the nature of dark matter remains an open question. While in the MSSM the only available TeV-scale dark matter candidate is the lightest neutralino \cite{5}, very weakly interacting dark matter particles might exist at much lower masses \cite{6}. In the light of many indirect constraints on neutralino–induced higher–dimensional operators we can extend the dark matter fermion to a Dirac spinor \cite{7}, predicting interesting but still unobserved signatures at the LHC \cite{8}. Recent years have seen a large effort to condense properties of different dark matter models into effective theory concepts \cite{9}. In spite of all these options we will limit ourselves to the case where the entire observed dark matter density is due to a single state, the lightest Majorana neutralino. If this hypothesis comes under experimental pressure, this might serve as a motivation for more elaborate dark sectors, but we will see that there is no such pressure.

Our analysis is based on the SFitter toolkit which determines the underlying parameters of complex models in the absence of simple one–to–one correlations of observables and parameters. We explore the parameter space with Monte Carlo Markov Chains of the likelihood function. This tool also permits to compare the results within the same framework, using either Bayesian or Profile Likelihoods analysis. It has previously been applied to the problem of the determination of supersymmetric parameters \cite{10}, including a bottom-up renormalization group analysis and experimental information on production rates \cite{11}, as well as Higgs coupling measurements \cite{12}. In this paper we will study the impact of the recent LHC Higgs measurements and of the $\Omega_{cdm} h^2$ measurement by Planck. We will compare the latter to the WMAP-9year results \cite{13}.

We will use mSUGRA \cite{14} as an illustration of the constraints than can be put through the use of this full set of measurements. This step is necessary to study what happens in models where the a-priori relatively unrelated weak dark matter sector, Higgs sector, and strongly interacting sector of the MSSM are strongly linked by a high-scale construction. The main emphasis of our study is the challenging study of a TeV-scale MSSM. The determination of its parameters is the ultimate goal in order to infer from data whether the parameters are unified at a higher scale. This determination should shed light on which scenarios of SUSY breaking might be favored \cite{15}. Therefore we use a 13 parameter MSSM, which is a technically challenging endeavor because of the large number of parameters. In addition we use the top mass as an input and as a parameter. This additional parameter helps fine tuning the Higgs mass for dark matter annihilation.

Similar studies have been performed by other groups considering different models: for instance, Fittino has studied the impact of LHC data and WMAP-7year results \cite{16} on two models, mSUGRA and a non-universal Higgs model, the MasterCode group has performed a likelihood study of the same mSUGRA and non-universal Higgs models including Xenon100 results \cite{17}. A specific analysis with Planck data, the Higgs mass measurement, and Xenon100 in the TeV-scale MSSM exists but which focuses on light neutralino dark matter \cite{18}. Results similar to ours have recently been published in Ref. \cite{19} for mSUGRA and by the BayesFITS group, including the study of a 9-parameter MSSM in Ref. \cite{20}. Compared to this model, we are letting the data constrain more parameters, rendering the determination more complex. A non-exhaustive list of other, similar analyses is given in Ref. \cite{21}.,
II. SUPERSYMMETRIC PARAMETERS

With the limited number of actual measurements entering this analysis it is clear that we will not be able to make any definite statements about a full TeV-scale supersymmetric mass spectrum. We will illustrate our results using two model setups. As a first test we will study the unified gravity-mediated mSUGRA model, this will give us some ideas about how strongly unified models can accommodate the various data constraints. Second, in a proper bottom–up approach we will consider a free TeV-scale spectrum, reduced to the subset of relevant mass parameters.

The strongly constrained mSUGRA model is described by three mass parameters defined at the unification scale: $m_0$, the common scalar breaking mass parameter, $m_{1/2}$ the common gaugino breaking mass parameter and $A_0$, the common trilinear mass parameter. In addition, $\tan \beta$ as the ratio of the vacuum expectation values of the two Higgs doublets encodes successfully electroweak symmetry breaking. Finally, we have to fix the sign of the higgsino mass parameter $\mu$. In our conventions the term $-\mu$ appears in the lower–right off-diagonal terms of the neutralino mass matrix. The off-diagonal entry in the stop mass matrix is $m_t (A_t - \mu \cot \beta)$ \cite{24}. Because the parameter $A_t$ is the key parameter in the computation of the light Higgs mass around 126 GeV we quote the approximate solution to the renormalization group evolution \cite{25},

$$A_t = A_0 \left(1 - \frac{0.75}{\sin^2 \beta}\right) - 3.5 m_{1/2} \left(1 - \frac{0.41}{\sin^2 \beta}\right) \approx \begin{cases} 0.62 A_0 - 2.8 m_{1/2} & \text{for } \tan \beta = 1 \\ 0.25 A_0 - 2.1 m_{1/2} & \text{for } \tan \beta \gg 1 \end{cases}. \quad (1)$$

The larger $\tan \beta$ becomes the more the weak-scale parameter $A_t$ is driven by $m_{1/2}$. For $m_{1/2} > 0$ we essentially almost find $A_t < 0$.

When we use renormalization group equations to run high–scale supersymmetry breaking parameters to the weak scale, fixed to 1 TeV as suggested by Ref. \cite{26}, we need to ensure that we successfully generate the observed electroweak symmetry breaking. It is convenient to include $\tan \beta$ as a mSUGRA model parameter, but this choice mixes high–scale mass parameters with a TeV–scale ratio of vacuum expectation values. To be more consistent in the definition of the mSUGRA parameter space we can avoid $\tan \beta$ and replace it with the appropriate mass parameters evaluated at the unification scale \cite{25},

$$\mu^2 = m_{H_u}^2 \frac{\sin^2 \beta - m_{H_d}^2 \cos^2 \beta}{\cos(2\beta)} - \frac{1}{2} m_Z^2,$$

$$2B\mu = (m_{H_d}^2 - m_{H_u}^2) \tan(2\beta) + m_Z^2 \sin(2\beta). \quad (2)$$

$H_u$ has a tree–level coupling to up–type fermions, while $H_d$ couples to down–type fermions. The parameter $B\mu$ accompanies the doublet mixing $H_u^0 H_d^0$. Instead of $m_{H_d}$ and $\tan \beta$ we can use $B$ and $\mu$ and the correct value of $m_Z$ as mSUGRA model parameters. For the profile likelihood approach the two parametrizations are equivalent. However, for the Bayesian approach they will lead to different priors and hence to different results \cite{13}. In terms of $\tan \beta$ a flat prior in the high–scale mass parameters corresponds to the prior \cite{27}

$$\left| \frac{m_Z}{2\mu^2} \left( m_{H_u}^2 + m_{H_d}^2 + 2\mu^2 \right) \frac{1 - \tan^2 \beta}{(1 + \tan^2 \beta)^2} \right|,$$

defined at the electroweak scale. At large values of $\tan \beta$, the Jacobian in Eq.(3) scales like $1/\tan^2 \beta$, which means that the high–scale flat prior prefers small values of $\tan \beta$. When we define the entire MSSM parameter set at the TeV–scale, Jacobians like the one shown in Eq.(3) are simply an effect of our freedom to choose our MSSM model parameters.

In computing the weak–scale mass spectrum in the simple mSUGRA model we start with the independent GUT–scale parameters, evolve the soft SUSY–breaking parameters to the TeV scale, and compute the corresponding masses of the supersymmetric states. SFitter primarily relies on SuSpect2 \cite{24} for the renormalization group evolution and the computation of the supersymmetric mass spectrum. In addition, we use SoftSusy \cite{28} to test our results. Because of the different behavior of the squark and the gaugino masses in the $m_0$ vs $m_{1/2}$ plane \cite{29} some complexity of the mSUGRA model arises through parameter correlations.
The most general MSSM contains a large number of parameters, of which we identify 17 which will affect current LHC and dark matter measurements \[13\]. Moreover, the absence of evidence for supersymmetric particles at the LHC leads us to effectively decouple some of the masses to values well about the TeV scale.

In this analysis all squark mass parameters with the exception of the stop sector are fixed at 2 TeV. The same value is assumed for the gluino mass parameter \(M_3\). This way gluinos and light–flavor squarks move outside the region excluded by the LHC. The question of the bias introduced by this assumption will be addressed later. The trilinear mass parameter \(A_0\) is assumed to be zero. The first–generation slepton parameters are identified with their second–observation counter parts. This leaves 13 supersymmetric parameters to be explored: \(\tan \beta\), the electroweak gaugino mass parameters \((M_1, M_2)\), the smuon and stau sectors \((M_{\tilde{\mu}_{L,R}}, M_{\tilde{\tau}_{L,R}}, A_t)\), the stop sector \((M_{\tilde{b}_{3L}}, M_{\tilde{b}_{R}}, A_t)\), the heavy Higgs mass \(m_A\), and the higgsino mass parameter \(\mu\).

Effectively, this reduced parameter space decouples the strongly interacting MSSM sector from the weak sector with the relevant dark matter and Higgs predictions. The only remaining strongly interacting particle in the picture is the top squark with its large impact on the Higgs sector — related to its particular relevance in the solution of the hierarchy problem. Since the uncertainties in the top quark mass are non-negligible, and because the induced parametric uncertainties for example for the light MSSM Higgs mass cannot be neglected, we include it as an additional model parameter in the mSUGRA as well as in the MSSM analysis.

The prediction of the light MSSM Higgs mass is calculated with SUSPECT2 \[24\] while the Higgs branching ratios are computed using SUSY-HIT and HDECAY \[30\]. The supersymmetric contribution to the cold dark matter density is calculated with MicroMegas \[31\]. For the electroweak precision observables we rely on SusyPope \[32\]. Finally, we use SUStect2 \[24\] and MICRO MEGAS \[31\] to compute the \(B\) observables and \((g - 2)_\mu\).

### III. ANNIHILATION CHANNELS

To study the effect of the measured dark matter relic density on the supersymmetric parameter space we need to take into account the fact that data drive us into a few distinct parameter regimes \[21\]. These structures combined with the light Higgs mass prediction will lead to well–defined regions of the mSUGRA and MSSM parameter spaces which are consistent with all current data.

The first is the light Higgs funnel region where the mass of the lightest Higgs boson is about twice the mass of the LSP. The leading contribution to dark matter annihilation is then the \(s\)-channel annihilation via the lightest Higgs, dominantly decaying to \(b\) quarks. As a consequence of the tiny width of the lightest Higgs, \(\Gamma_h \sim 5\) MeV, the LSP mass has to be finely adjusted to produce the correct range in \(\Omega_{\text{cdm}} h^2\). A small, \(\mathcal{O}(10\%)\) higgsino component of the LSP will give the correct relic density. Technically, this precise tuning will be a challenge for our parameter analysis.

The same \(s\)-channel annihilation can proceed via the heavy Higgs bosons \(A, H\), where the widths can be very large and the level of tuning will be smaller. Unlike the \(h\)-funnel, this \(A\)-funnel region can extend to arbitrarily large LSP masses, provided the Higgs masses follow the LSP mass. The main heavy Higgs decay channels are \(bb\) and \(\bar{t}t\), because, in these kinds of two-Higgs-doublet models, the massive gauge bosons decouple from the heavy Higgs sector.

A second annihilation topology gives rise to the \(\tau\) co-annihilation region \[33\]. Here, the mass difference between for example the stau as the next-to-lightest supersymmetric particle and the LSP needs to be small, of the order of few per-cent or less. If the LSP has a large higgsino component the annihilation then proceeds via an \(s\)-channel tau lepton into a tau and a pseudo–scalar Higgs. On the scale of the size of LHC detectors the stau could in such scenarios become stable. However, the higgsino component is not required for \(\tau\)-co-annihilation to work. If instead the selectron or smuon are the next-to-lightest supersymmetric particles and essentially mass degenerate with the LSP they could lead to the same effect. In the squark sector the same mechanism exists for the lightest top squark \[34\] or other squark next-to-lightest superpartners. However, given the preference of the Higgs mass measurement for heavy stop masses we find it outside our preferred parameter range.

In the absence of a significant mass splitting between the lightest neutralino and lightest chargino, co-annihilation in the neutralino–chargino sector can accelerate dark matter annihilation in the early universe \[35\]. Because the necessary mass degeneracy cannot appear for a light bino, the LSP will be dominantly wino or higgsino. Two final states occur for neutralino–chargino co-annihilation: if the \(t\)-channel neutralino or chargino exchange dominates, massive gauge bosons and eventually light–flavor quarks will be produced in the
annihilation process. If, in contrast, a heavy Higgs in the $s$-channel dominates, the final state will dominantly consist of third-generation quarks.

Finally, the focus point region $^{23, 50}$ is characterized by large $m_0$, small $m_{1/2}$, and accidentally small $|\mu|$. Close to this region of parameter space where $\mu$ changes sign, we find a higgsino-like light neutralino which couples to gauge bosons and can annihilate into the $W W$ channel. For mSUGRA, this area is highly reduced by both Xenon100 $^{19}$ and LHC gluino search limits $^{37, 38}$.

### IV. DATA AND ANALYSIS SETUP

In Table I we list the main experimental inputs to our analysis. The Higgs mass measurement at the LHC considered in this study is from ATLAS $^{39}$. Because it comes with a sizeable theoretical error from the supersymmetric prediction an improved measurement, such as the measurement of $BR(B_s \to \mu^+\mu^-)$ by CMS $^{41}$, will not affect our results. The different production and decay channels of the Higgs boson $^{45}$ provide some additional information on its couplings $^{12}$, but with little impact on the supersymmetric parameter space when added to the Higgs mass and the flavor observables $^{40}$. We consider the updated result $BR(B_s \to \mu^+\mu^-) = (2.9^{+1.1}_{-1.0} \pm 0.2) \times 10^{-9}$ $^{47}$ in the mSUGRA section. It has no impact on the results so we stick to the value quoted in Table I for the MSSM study.

A major point of this study is on the new measurement of the cold dark matter density of the universe by the Planck collaboration. We compare it with the WMAP-9-year measurement. In both cases we use the values from the more precise measurements in the ΛCDM scenario:

- Planck: $\Omega_{cdm} h^2 = 0.1187 \pm 0.0017$ $^{4}$
  This is a combination of Planck data, large scale polarization WMAP data $^{48}$, ACT/SPT $^{49}$, and baryon acoustic oscillation measurements (BAO) $^{50}$.

- WMAP-9-year: $\Omega_{cdm} h^2 = 0.1157 \pm 0.0023$ $^{16}$
  This combines WMAP data, BAO and a Hubble parameter measurement $^{51}$.

Some tension remains between Planck’s estimated $H_0$ value and the direct measurements used in the WMAP-9-year analysis. We compare the two approaches to see whether the difference in central values and errors leads to differences in the constraints on the supersymmetric parameter space.

An additional dark matter related input is the upper limit on the elastic LSP–Nucleon cross section as function of the LSP mass from the analysis of the Xenon100 225 days $\times$ 34 kg dataset $^{12}$.

For $\tan \beta > 50$ the branching ratio of the flavor violating decay $B_s \to \mu^+\mu^-$ is particularly sensitive to supersymmetric contributions $^{52}$ and hence constraining. The measurement of $BR(b \to X_s\gamma)$ tends to disfavor $\mu < 0$ for large $\tan \beta$ $^{53}$. The difference in the predicted and measured anomalous magnetic moment of the muon tends to accommodate large $\tan \beta$ and to disfavor $\mu < 0$ $^{54}$. The reason for this definite sign preference in $\mu$ is a possible cancellation in the off-diagonal entries of the third generation scalar mass matrices. The top mass $^{44}$ is both, a model parameter and a measurement.

| measurement | value and error |
|-------------|-----------------|
| $m_h$ | $(126 \pm 0.4 \pm 0.4 \pm 3) \text{ GeV}$ $^{39}$ |
| $\Omega_{cdm} h^2$ Planck | $0.1187 \pm 0.0017 \pm 0.012$ $^{4}$ |
| $\Omega_{cdm} h^2$ WMAP-9year | $0.1157 \pm 0.0023 \pm 0.012$ $^{16}$ |
| $BR(B_s \to \mu^+\mu^-)$ | $(3.2^{+1.7}_{-1.2} \pm 0.2) \times 10^{-9}$ $^{40}$ |
| $BR(b \to X_s\gamma)$ | $(3.55 \pm 0.24 \pm 0.09) \times 10^{-4}$ $^{42}$ |
| $\Delta a_\mu$ | $(287 \pm 63 \pm 49 \pm 20) \times 10^{-11}$ $^{43}$ |
| $m_t$ | $(173.5 \pm 0.6 \pm 0.8) \text{ GeV}$ $^{44}$ |

**TABLE I**: Some of the key measurements used in our analysis, including the error. The last number is the theoretical uncertainty on the supersymmetric prediction, except for the $BR(b \to X_s\gamma)$ and $m_t$ for which no theoretical uncertainty is considered.
In SFitter the statistical errors on the measurements are treated as Gaussian or Poisson where appropriate. The systematic errors are correlated if originating from the same source. Theoretical uncertainties are treated with the Rfit scheme \cite{13, 15, 55}, i.e. using flat errors in a profile likelihood construction.

The analysis proceeds in two steps. First, we construct a fully exclusive log-likelihood map in the model parameters using a set of Markov Chains with a Breit-Wigner proposal function. Each chain has a different starting point. Their convergence is checked by comparing the mean values and variances of each chain through the quantity $\hat{R}$ \cite{56} as implemented in Ref. \cite{57}. The maximum over the set of Markov Chains $\max[\hat{R}]$ will approach unity if the chains have converged and cover the full parameter space.

On this exclusive log-likelihood map we then define two types of projections: a profile likelihood based on the Frequentist approach and a marginalization as an example of the Bayesian approach. The absolute scales of the projected log-likelihood values in the two approaches cannot be used to compare them.

In 2-dimensional standard contour plots we identify the interesting parameter regions and their correlations. In these regions we explore the structures locally, using a modified version of Minuit \cite{58} to refine the location of the minima.

V. MSUGRA ANALYSIS

The strongly constrained mSUGRA parameter space is governed by a very small number of parameters. They are linked to the TeV-scale masses via coupled renormalization group running and therefore highly correlated. Knowing the light Higgs mass further constrains the parameter space through the stop sector. In such cases the standard Markov Chain Monte Carlo methods give the most stable results, so we do not use the weighted Markov Chains which are otherwise optimized for a small number of parameters \cite{13, 59}. For each sign of $\mu$ we travel in the 5-dimensional parameter space of $m_0$, $m_{1/2}$, $A_0$, $\tan\beta$, and $m_t$ with 49 Markov chains of 200000 points each, giving us 9.8 million accepted samplings. Our parameter space is bounded by $m_0 < 5$ TeV, $m_{1/2} < 5$ TeV, $|A_0| < 4$ TeV, and $\tan\beta < 61$. The convergence criterion finds $\max[\hat{R}] \approx 1.008$, indicating a good convergence of the chains.

A. Profile likelihood for positive $\mu$

Because a priori the sign choice $\mu > 0$ is favored by the $\Delta a_\mu$ measurement, we will discuss it first. The four different 2-dimensional profile likelihoods for $\mu > 0$ are shown in Figure \ref{fig:profile}. All of them use the recent Planck measurement of the cold dark matter density. The first observation is the absence of a clear preference in the $m_0$ values. In contrast, the dark matter relic density favors three distinct regions in $m_{1/2}$, as introduced in Section III:

1. the narrow stau co-annihilation strip with $m_{1/2} < 1$ TeV and $m_0 < 500$ GeV at moderate $\tan\beta$. The mass of the lightest slepton $\tilde{\tau}_1$ is very close to the LSP mass.

2. the $A$-funnel region with $m_{1/2} \approx 1.7$ TeV and $\tan\beta \approx 50$, where the LSP mass around 745 GeV is roughly half the heavy Higgs mass $m_{A,H}$ and the heavy Higgs states have a sizeable width to allow for a spread-out $s$-channel annihilation.

3. the $h$-funnel region with $m_{1/2} \approx 130$ GeV, where the bino-LSP mass of 60 GeV is about half the mass of the lightest Higgs. The dominant dark matter annihilation process is the resonant $s$-channel annihilation via the lightest Higgs boson. Because of the link between the LSP and gluino masses, this channel could typically be ruled out by direct LHC searches.

Two additional well-known parameter regions \cite{21} are explicitly excluded by our bounds of the parameter space. We nevertheless confirm that they would appear in an extended parameter scan, namely

4. the focus point region \cite{25, 36} with its $WW$ annihilation channel at $m_0 \in [3, 20]$ TeV, and $m_{1/2} \in [0.2, 20]$ TeV. This region is mainly excluded by Xenon100 \cite{19}, except for a few points such as SPS2 \cite{60} which is ruled out by LHC exclusions \cite{37, 38}.

5. the stop co-annihilation strip with $A_0/m_0 \in [3, 6]$ and $A_0/m_0 \in [-15, -3]$. 

In particular the size of the $A$-funnel region is then defined by the light Higgs mass constraint. Relating the Higgs mass constraint we need to be a little careful. In Section II we have seen that the relevant trilinear coupling $A_t$ mostly scales with $m_{1/2}$. The main contribution to the light Higgs mass comes from the two top squarks, so the relatively heavy Higgs mass pushes the preferred physical stop masses to large values. According to Eq.(1) negative values of $A_0$ will increase $|A_t|$, leading to a larger stop mass splitting and hence a smaller mass of the lighter stop mass eigenstate. Indeed, we find that the different measurements prefer $A_0 > 0$, while large negative $A_0$ values and low $m_0$ values are disfavored by the Higgs mass constraint.

In the lower panels of Figure 1 we see that large tan $\beta$ values are clearly favored, independently of $m_0$. An exception appears only for large $m_0$ values, where the allowed range in tan $\beta$ becomes sizeable. The dark blue area for 500 $\lesssim m_0 \lesssim$ 3000 GeV and tan $\beta < 35$ is disfavored by the Higgs mass measurement. Large values of tan $\beta$ are needed to increase its value, while the stop masses are fairly independent of $m_0$. Dark matter plays the key role in excluding the white area around $m_0 \approx 3.5$ TeV.

| Region      | $m_0$    | $m_{1/2}$ | tan $\beta$ | $A_0$  | $m_t$  | $-2\log L$/dof (LHCb) |
|-------------|----------|-----------|--------------|-------|-------|------------------------|
| co-annihilation | 442     | 999       | 24.6         | -1347 | 174.0 | 49.0/75                |
| $A$-funnel   | 1500    | 1700      | 46.5         | 2231  | 173.9 | 48.9/75                |
| $h$-funnel   | 4232    | 135       | 26.6         | -2925 | 174.2 | 46.1/75                |

TABLE II: Illustration of best-fit parameters for the three regions of mSUGRA: $A$-funnel, $h$-funnel, and co-annihilation with $\mu > 0$. The corresponding $-2\log L$ is given in column 7. The last column illustrates the impact on the new LHCb measurement of BR($B_s \rightarrow \mu^+ \mu^-$).
A similar feature, albeit a small anti-correlation, can be seen in the \( m_{1/2} \) vs \( \tan \beta \) plane. The slight anti-correlation for large \( \tan \beta \) and \( m_{1/2} \) is attributed to the Higgs masses. First, the light Higgs mass increases with a larger stop mass and hence growing \( m_{1/2} \), so smaller values of \( \tan \beta \) become possible. Moreover, the dark matter relic density can be reached through the pseudoscalar annihilation funnel. Because a decrease of \( \tan \beta \) increases the heavy Higgs masses, the dark matter relic density forces a simultaneous increase in \( m_{1/2} \) and hence the LSP mass. This keeps the mass ratio around 2:1.

In Table III we show the best-fit solutions in the mSUGRA parameter space. In the last column we compare the log-likelihood obtained with the updated measurement of \( \text{BR}(B_s \to \mu^+ \mu^-) \) showing that the results do not depend on this observable. The three preferred regions with their distinct dark matter annihilation processes are kept separate. For the \( A \) and \( h \) funnels in mSUGRA the LSP has roughly the same gaugino–higgsino composition. It is dominantly a bino and annihilates to \( b \bar{b} \) final states. In the co-annihilation point the annihilation goes into \( \tau \tau \) final states, helped by the process \( \tilde{\tau} \tilde{\chi}^0_1 \to A \tau \). The general preference for large \( m_{0} \) values from the dark matter constraints and the lightest Higgs mass overrides the favorite regions for \( (g-2)_\mu \), which until recently dominated the corresponding analyses. The \( \Delta \delta_\mu \) contribution to \(-2 \log L\) becomes a constant offset.

The influence of the top mass and its uncertainty cannot be neglected, as we see for example in the \( h \)-funnel region. Compared to the nominal value of 173.5 GeV in Table II the best fit result shown in Table III is increased by 0.7 GeV. This increase leads to a slight reduction of \( M_1 \) by at most 0.1 GeV and an increase of \( \mu \) from 350 GeV to 490 GeV. For the LSP this implies a larger mass by about 0.8 GeV and a decreased higgsino component by almost 50%. In parallel, the Higgs mass increases by 0.2 GeV, as compared to the prediction using the nominal top mass. Combining the two mass shifts and the decreased LSP coupling to the Higgs leads to the correct value of \( \Omega_{\text{cdm}} h^2 \).

The complete mass spectrum of the particles corresponding to the three points is given in Table III. The \( h \)-funnel has a relatively light gluino of 476 GeV, driven by the low LSP mass. The squark masses turn out heavy. Because the available mSUGRA limits from ATLAS [37] and CMS [38] are calculated for different values of \( A_0 = 0 \) and \( \tan \beta = 10 \) the results cannot be applied directly, but it is clear that this parameter point will be excluded by inclusive squark and gluino searches at the LHC. The only obvious way to hide light gluinos in these analyses would be to complement them with mass-generate squarks, such that the decay jets become too soft to be observed [67]. However, in mSUGRA the squark masses are linked to the stop masses, and light stop masses are ruled out by the Higgs mass constraint. Hence, for mSUGRA the list of non-excluded dark matter annihilation channels given in Section III is reduced to stau co-annihilation and the \( A \)-funnel within the parameter space considered in this analysis.

As mentioned above, one of the key motivations of this analysis is to see the impact of the recent Planck measurements, in comparison to the WMAP-9year results. The most visible difference can be observed in the \( (m_{1/2}, A_0) \) plane in Figure 2. The general features are very similar. In addition, the separation between the light Higgs funnel region and the rest of the plane becomes clearer with the new and improved Planck measurement. This reflects the essentially equivalent central values but smaller error bars on \( \Omega_{\text{cdm}} h^2 \).

| co-ann. \( A \) | \( h \) | co-ann. \( A \) | \( h \) | co-ann. \( A \) | \( h \) |
|----------------|------|----------------|------|----------------|------|
| \( \tilde{e}_L \) | 792  | 1860 | 4210 | \( \tilde{g} \) | 2178  | 3596 | 476 |
| \( \tilde{e}_R \) | 575  | 1621 | 4223 | \( \tilde{H}_L \) | 429   | 745  | 59  |
| \( \tilde{e}_R \) | 788  | 1858 | 4209 | \( \tilde{H}_L \) | 809   | 1379 | 118 |
| \( \tilde{\mu}_L \) | 792  | 1860 | 4210 | \( \tilde{H}_L \) | -1407 | -1588 | 507 |
| \( \tilde{\mu}_R \) | 575  | 1621 | 4223 | \( \tilde{b}_2 \) | 1412  | 1603 | 512 |
| \( \tilde{b}_1 \) | 788  | 1858 | 4209 | \( \tilde{b}_2 \) | 810   | 1379 | 119 |
| \( \tilde{\tau}_1 \) | 430  | 1103 | 3920 | \( \tilde{\tau}_2 \) | 1412  | 1603 | 514 |
| \( \tilde{\tau}_2 \) | 756  | 1666 | 4062 | \( \tilde{\nu}_R \) | 744   | 1661 | 4061 |

TABLE III: Supersymmetric particles’ masses (in GeV) for the three best–fit points shown in Table II. They correspond to the favored regions: \( A \)-funnel, \( h \)-funnel, and co-annihilation with \( \mu > 0 \).
B. Bayesian probability for positive $\mu$

To this point we have only relied on profile likelihood projections. While Frequentist and Bayesian approaches cannot be expected to give equivalent answers (because they ask different questions) they can still give complementary information. In Figure 3 we show the Bayesian projections onto the $(m_0, m_{1/2})$ and $(m_0, \tan \beta)$

FIG. 2: Profile likelihood projection onto the $(m_{1/2}, A_0)$ plane using the Planck (left) and WMAP (right) measurements.

FIG. 3: Bayesian projection onto the $(m_0, m_{1/2})$ plane (left) and the $(m_0, \tan \beta)$ plane (right) for a $\tan \beta$–flat prior (top) and a high–scale flat prior (bottom). All results are based on the Planck measurement and assume $\mu > 0$. 
planes, using the consistent tan $\beta$–flat and high–scale flat priors discussed in Section III.

Both, the $(m_0, m_{1/2})$ plane and the $(m_0, \tan \beta)$ plane using the consistent high–scale flat prior show similar features as for the profile likelihood approach. First, there is the well separated low–$m_{1/2}$ solution from the light Higgs funnel. Second, the narrow co-annihilation strip is hard to see, but still present. Finally, the $A$-funnel bulk region is divided in low and high $m_0$ values and shows a clear preference for $m_0 > 4.5$ TeV and $m_{1/2} \approx 2.8$ TeV. This can be explained by the volume effect when integrating over $\tan \beta$, $A_0$, and $m_t$: the best-fit value around $m_{1/2} = 1.5$ TeV has a low probability for most $\tan \beta$ values, except for $\tan \beta = 40–50$. In contrast, for $m_{1/2} \approx 2.5$ TeV the preferred region extends over almost all $\tan \beta$ values. In general, $m_t$ moves significantly below its nominal value to accommodate the $A$-funnel region, but covering a larger range for large $m_0$. All of these features can also be seen in the profile likelihood analysis, but they only develop two well defined preferred regions after we integrate the Bayesian probabilities.

The whole picture changes significantly when we instead use a low–energy prior, flat in $\tan \beta$, in the Bayesian analysis. In the $(m_0, m_{1/2})$ plane the low-$m_0$ part of the bulk solution vanishes. In the $(m_0, \tan \beta)$ plane, suddenly low $\tan \beta$ values are favored. This is simply an effect of the relative difference in priors shown in Eq.(3). Such a prior dependence suggests that our information is not yet sufficient to draw conclusions on Bayesian favored regions.

C. Negative $\mu$

Finally, we turn to $\mu < 0$. From the argument above we would expect similarly good fits with a finite log-likelihood offset from $\Delta a_\mu$. In Figure 4 we indeed observe similar features as for $\mu > 0$, but on the absolute scale of the log-likelihood only the $h$-funnel region at low $m_{1/2}$ retains its features. The $A$-funnel region at $m_{1/2} \approx 1.5$ TeV is now clearly disfavored.

The correlation in $\tan \beta$ vs $m_0$ sheds some light on this feature: for large values of $\tan \beta$ and $\mu < 0$ values the cancellation in the off–diagonal entries of the third generation squark mass matrices fails. This will lead to light sbottoms and stops with very large couplings to the heavy Higgs states. They will trigger conflicts with heavy flavor measurements and eventually with the perturbativity of the renormalization group equations. The best solutions for $\mu < 0$ are hence restricted to the light Higgs funnel and the co-annihilation regions at low values of $m_{1/2}$.

VI. MSSM ANALYSIS

Going from a strongly constrained model such as mSUGRA to the MSSM increases the number of free parameters. The ultimate goal of such an analysis is to shed light, with enough experimental constraints, on which scenarios of SUSY breaking are favored. We choose to constrain 13 parameters plus the top mass.
Our parameter space is bounded by \( \tan \beta < 61 \), \((M_1, M_2) < 4 \text{ TeV}, (M_{R_{L/R}}, M_{R_{L/R}}, M_{Q_{L/R}}, M_{L_{R}}) < 5 \text{ TeV}, (|A_{\tau}|, |A_{t}|) < 4 \text{ TeV}, m_A < 5 \text{ TeV} \) and \(|\mu| < 2 \text{ TeV}\). This number is considerably larger than the number of strong constraints or measurements we apply in our analysis, rendering the analysis quite complex in terms of likelihood maximization. On the other hand, now, different sub-sectors of parameters largely decouple. We analyze the MSSM parameter space with 100 Markov chains of 200000 points each, leading to a total number of \( 2 \times 10^7 \) of tested samples. For the convergence parameter \( \max[\hat{R}] \) typical values are 1.005 and better.

The measured light Higgs mass essentially depends on three parameters: the heavy Higgs mass scale \( m_A \), which has to be large to accommodate the 126 GeV measurement; \( \tan \beta \) which has to be large enough to not delay the decoupling regime in \( m_A \); and finally the geometric mean of the two stop masses \( \sqrt{m_{\tilde{t}_1}m_{\tilde{t}_2}} \), which again has to be large. In terms of MSSM parameters the latter needs to be computed from the three entries in the stop mass matrix, including \( A_t \). The stop masses are the key parameters, but are neither strongly related to the dark matter sector nor to the light–flavor squark–gluino mass plane. In addition, they are directly linked to the solution of the hierarchy problem and hence to the motivation of supersymmetry.

The light–flavor squark masses and the gluino mass are experimentally constrained by searches for jet plus missing energy in LHC experiments. While it is entirely possible to avoid these limits in certain decay setups, the strongly interacting supersymmetric masses are likely to lie in the several-TeV range. This tendency towards a heavy strongly interacting SUSY sector is in line with the stop mass constraint from the Higgs sector.

The dark matter sector is most strongly constrained by our requirement that the entire relic density is due to the LSP, in our case the lightest neutralino. The neutralino masses and couplings depend on the four parameters \( M_1, M_2, \tan \beta \) and \( \mu \). The link between the dark matter sector and other sectors rests on the different LSP annihilation channels, as explained in detail in the mSUGRA section. For a sufficiently fast LSP annihilation we cannot rely on generic scattering processes, for example with a \( t \)-channel slepton, squark, or chargino. Instead, the easiest ways to reach the observed \( \Omega_{\text{cdm}} h^2 \) values are light and heavy Higgs funnels and co-annihilation.

In general, the range of \( \mu \) is strongly limited as the light charginos and neutralinos are constrained by direct LEP searches and \( Z \) pole measurements \[62\]. This results in log-likelihood values about ten times worse than the minimum. For example, for \( \mu = 20 \) GeV and variable \( M_2 \) the typical \( Z \) width is increased by 30 MeV, a large amount compared to the error of 3 MeV and hence ruled out.

In Figure 5 we show the profile likelihoods in the neutralino and chargino sector \( M_1, M_2, \) and \( \mu \) for the Planck measurement. All measurements discussed in Section IV are included. The log-likelihood map favors five regions, three of which directly correspond to the mSUGRA case:

1. the stau co-annihilation strip diagonal in \( M_1 \) vs \( M_2 \) at relatively small values. Here, the mass of the lightest slepton \( \tilde{\tau}_1 \) is very close to the LSP mass.

![FIG. 5: Profile likelihood projection onto the \((M_1, M_2)\) plane (left) and the \((M_1, M_2)\) plane (right) for the Planck measurements.](image)
As for the mSUGRA case an additional stop co-annihilation region exists, but is not covered by our parameter range.

2. the A-funnel region where the LSP mass is about half the heavy Higgs mass. This MSSM region behaves the same way as discussed for the simpler mSUGRA model. In Figure 5 it contributes to the bulk region of the $M_1$ vs $M_2$ plane as well as to the correlated patterns in the $M_1$ vs $\mu$ plane.

3. the h-funnel region at low $M_1 \sim 63$ GeV almost independent of $M_2$. Unlike for mSUGRA the gluino mass is now an independent parameter, so the direct LHC searches decouple from the dark matter sector. Because the corresponding MSSM parameter space is tiny, the funnel appears only as distinct sets of points in Figure 5. We have checked that it actually is a narrow line.

4. a bino-higgsino region which appears as a strip in the $M_1$ vs $\mu$ plane for $\mu < 0$ and $|M_1| \approx |\mu|$. The dark matter annihilation proceeds through different neutral and charged Higgs–mediated channels, including chargino co-annihilation and dominantly third–generation quarks in the final state. The latter includes the $b\bar{b}$ final state from the A-funnel.

5. a large higgsino region with $M_1, M_2 > 1.2$ TeV, split in two almost symmetric solutions $\mu \approx \pm 1.2$ TeV. Because the LSP characteristics in the two regions are very similar we will only refer to $\mu > 0$. Chargino co-annihilation dominates the prediction of the relic density with first and second generation quarks in the final state.

As for the mSUGRA case an additional stop co-annihilation region exists, but is not covered by our parameter range.

In Table IV we give examples for individual best-fitting parameter points in each of these regions. As the parameters are less correlated in the MSSM than in mSUGRA, the top quark mass parameter essentially does not move from its measured value. None of these points are excluded from LHC direct SUSY Higgs searches such as [62]. For the bulk of the solutions the hierarchy in the neutralino sector favors a smaller $\mu$, corresponding to a LSP with a strong higgsino component. Such solutions are hardly realized in strongly constrained models like mSUGRA.

Nevertheless, as every mSUGRA parameter set is contained in the full MSSM, it is important to check that the additional MSSM parameters do not have a large effect on the predictions for the observables and the results of the minimization procedure. For example, the MSSM stau co-annihilation point is similar to the corresponding mSUGRA point: the gaugino mass parameters $M_1$ and $M_2$ are the values obtained after the renormalization group evolution from the GUT scale to the electroweak scale, as expected. The MSSM generalization of the A-funnel region shows a similar behavior. The most sensitive measurements are the Higgs boson mass and $\Omega_{\text{cdm}}h^2$, and both are within the theoretical error band. In the h-funnel scenario, $\Omega_{\text{cdm}}h^2$ is very sensitive to the exact value of the Higgs boson mass, the change to the fixed MSSM parameters leads to a change of 150 MeV of the Higgs mass and an increase of $\Omega_{\text{cdm}}h^2$. The bino–higgsino region does not
exist for the mSUGRA model. It is a generalization of the $A$-funnel, including chargino co-annihilation via a charged Higgs in the $s$-channel. Essentially mass-degenerate light neutralinos and charginos only appear for light winos or light higgsinos, both not within the range of the renormalization group equations starting from degenerate gaugino masses. For the same reason the higgsino LSP point with chargino co-annihilation through gauge bosons and into light quarks is also absent in the simplified mSUGRA model.

Exploring the MSSM for negative values of $M_1$ leads to similar structures in the $(M_1, M_2)$ and $(M_1, \mu)$ planes. To be precise, while for the $(M_1, M_2)$ plane we observe a mirror symmetry with respect to the $M_2$ axis, for the $(M_1, \mu)$ plane we see a symmetry with respect to a simultaneous change of sign of both $M_1$ and $\mu$. This observation is corroborated by the study of the parameter sets of Table IV if only the sign of $M_1$ is changed, the solution becomes less probable. If additionally the sign of $\mu$ is inverted, the mirror solution is as good as the original one. As the neutralino mixing matrix depends on $\mu$ and $M_1$, a simultaneous change of sign is equivalent to an unobservable global phase for the solutions considered here.

In Figure 6 we show the same parameter constraints as before, but for the WMAP measurement of the relic density. In the $(M_1, M_2)$ plane only a hint of a difference is visible, as WMAP allows for slightly lower $M_2$. In the $(M_1, \mu)$ plane, WMAP is more compatible in a slightly wider range than Planck with the thin bino–higgsino region identified in Figure 5 (right). On the other hand, WMAP gives slightly looser constraints for larger $\mu$ in the higgsino LSP scenario for negative $\mu$. In addition, the $h$-funnel region is less constrained by the WMAP measurement than by Planck.

As for the mSUGRA analysis, we also compare the profile likelihood with a Bayesian approach. Volume effects can now affect the determination of the model parameters, particularly changing the balance between small and large parameter regions like the $h$-funnel vs the higgsino regime. As shown in Figure 7, the higgsino LSP region is indeed identified the same way as in the Frequentist projection. The other solutions are more sensitive to volume effects and therefore washed out.

VII. OUTLOOK

Using SFitter we have studied the impact of measurements coming from cosmological studies ($\Omega_{cdm} h^2$), direct dark matter searches (Xenon100), and collider measurements (Higgs mass) on the parameter space of the mSUGRA model and on the TeV-scale MSSM. Additional direct and indirect constraints have been included in the analysis, but turned out to be secondary in defining the features of the preferred parameter regions.

We have compared the impact of the measurements of the dark matter relic density by Planck and by WMAP, indicating a very slight shift in the best–fitting parameter points. In contrast, a comparison of profile likelihood and Bayesian methods to reduce the multi–dimensional parameter space showed significant differences, arising
from volume effects and choice of prior. The latter can be chosen either at the GUT scale or at the TeV scale, giving rise to a Jacobian scaling like $\tan^2 \beta$.

The allowed regions of supersymmetric parameter space can best be categorized by the dark matter annihilation channel. In mSUGRA we found two valid regions, a narrow stau co-annihilation region at moderate $\tan \beta$ and a large $A$-funnel region. Stop co-annihilation survives the light Higgs mass constraint, but resides outside our tested range of model parameter space, while the focus-point region seems to be ruled out.

In the TeV-scale MSSM we found narrow allowed regions corresponding to stau co-annihilations and the light–Higgs funnel annihilation. The heavy Higgs funnel becomes part of a large parameter region where the lightest neutralino is a mixed bino–higgsino state, annihilating to third–generation fermions. Chargino co-annihilation occurs with a charged Higgs funnel. In addition, we observed a large higgsino region with chargino and neutralino co-annihilation through gauge boson and into light–flavor quarks. Finally, stop co-annihilation again resides outside our range of model parameters.

Because the allowed regions are very different in size, the Bayesian analysis becomes sensitive to volume effects in comparing dark matter annihilation channels. Moreover, in the light of these categories it is not clear how we would define a simple effective theory covering all these different supersymmetric scenarios, pointing towards a more complex set of effective dark matter models.

In terms of the supersymmetric Lagrangian we found that the positive measurements like the relic density or the Higgs mass generally push supersymmetry toward a high new physics mass scale. The absence of signals for new physics at the 8 TeV run of the LHC puts little tension into the parameter analysis. Nevertheless, several of the parameter regions corresponding to different dark matter annihilation can be probed by the LHC running at 13 TeV. While there is a generic benefit to testing a large variety of dark matter models, the successful simple mSUGRA analysis indicates that there is no immediate need for abandoning the standard WIMP hypothesis for the upcoming LHC run.

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