Path Planning Based on Fuzzy Decision Trees and Potential Field

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ABSTRACT

The fuzzy logic algorithm is an artificial intelligence algorithm that uses mathematical logic to solve problems by generating data values that are not precise in order to reach an accurate conclusion. In this work, Fuzzy decision tree (FDT) has been designed to solve the path planning problem by considering all available information and making the most appropriate decision given by the inputs. The FDT is often used to make a path planning decision in graph theory. It has been applied in previous research in the field of robotics, but it still shows drawbacks in that the agent will stop at the local minima and is not able to find the shortest path. Hence, this paper combines the FDT algorithm with the potential field algorithm. The potential field algorithm provides weight to the FDT algorithm which enables the agent to successfully avoid the local minima and find the shortest path.

Keyword:
Fuzzy Decision Trees
Local minima
Non-Holonomic
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1. INTRODUCTION

In general, mobile robot navigation which moves in dynamic environments has a major issue namely path planning [1]. In path planning problems, the mobile robot requires algorithms to find a safe path to avoid a collision and needs an optimal path in achieving the targets in the unknown environment [2]. A graph theory algorithm for path planning is needed to overcome the problems.

There are three types of graph theories, namely visibility, Voronoi, and cell decomposition graphs. Some researchers such as Liu and Zhang [3] have conducted path planning research by using the theories. The Voronoi diagram for the UAV path planning has been used. By using a global view, this graph splits equally large distance between obstacles in that the path for UAV is obtained. With the path, the UAV is able to head to the point of destination, but by applying merely this algorithm, the robot is not able to pass the local minima. Local minima a condition that makes robot stops at many obstacles.

The visibility graph algorithm was used by Jandt et al. [4] for mobile robot path planning. This algorithm connects not only the angles of one obstacle to another but also the angles to the initial and destination points of the robot. With this algorithm, the mobile robot is able to move to the destination point in the safest path but regrettably by applying this algorithm, the robot is not able to pass the local minima.

The cell decomposition was used by Ryan [5]. This algorithm divides the environment into small grids. The grids are used to find the safest path for multi-robot. The multi-robot heads to the destination point by using the grid lines. Graph theory is used for planning the safest path. The weakness of the algorithm that it is not able to find the shortest path.

With the remaining problems, some researchers have combined the graph theory with some algorithms such as Dijkstra's algorithm by Feuerstein and Marchetti-Spaccamela [6]. This algorithm has been
applied for planar path planning graph theory. By using this algorithm, the robot is able to find the shortest path. This algorithm was also implemented by Peyer et al [7] to search the shortest path in very large scale integration (VLSI).

The drawback of the Dijkstra’s algorithm is that it is not able to detect obstacles when applied to the mobile robot path planning. It has been modified by Liu et al [8] by combining it with the Floyd algorithm. The Floyd algorithm is used to detect obstacles while the Dijkstra algorithm is used to find the shortest path.

Other algorithms such as A* can also determine the shortest path. This algorithm has been applied by Cheng Liping et al [9] to find a parking lot, but it is also not able to detect moving obstacles. The A* and Dijkstra's algorithms were not able to detect obstacles, thus the two algorithms were combined with the artificial intelligence algorithm to detect them. In order for A* algorithm to be able to be applied to a mobile robot, the algorithm has been modified by Duchoň et al [10] by adding phi algorithm.

In addition to Dijkstra’s algorithm, the researcher has modified the cell decomposition graph theory into the tree graph theory [11]. Graph theory is often used to search for the fastest path. This theory has been supported by a decision support system by using fuzzy algorithm. This algorithm has been widely used to search data and decision makers [12]-[15]. In addition, the fuzzy algorithm has been used as a search path and to make a decision to find the shortest path. Many researchers have applied this algorithm as the search algorithm such as GH Shah Hamzei et al [16]. They use this algorithm for global planning.

The Fuzzy Decision Tree algorithm faces a problem when applied to the environment which has many obstacles. At many scenario, the agent will stop at a local minima and is not able to find the shortest path. Based on the problems, this paper combines the Fuzzy Decision Tree algorithm with potential field algorithm. The potential field algorithm provides weight to the fuzzy decision tree algorithm. With the given weight, the agent is expected to avoid local minima and determine the shortest path.

2. RESEARCH METHOD

Path planning is an algorithm that solves the problem of moving an agent from an initial to a goal position by passing obstacles. A research method by merging several path planning algorithms presented this paper are graph theory, fuzzy decision tree, and the potential field algorithms.

2.1. Graph Theory Algorithm

This paper presents global path planning method to establish an environmental model. Global path planning obtains data information that is the size of the environment and the data used for path planning such as agent position, position of obstacles and goal position as shown in figure 1. It shows that in the environment there is an initial position denoted by a blue star, a position of obstacle denoted by a red circle and a goal position of agent denoted by a small blue circle. The environment model is divided into grids which have same size.

![Figure 1. Environment modeling with cell decomposition](image-url)
the agent, \((X_G, Y_G)\) is the goal position of the agent, \(l_l\) is length of the grid, \(l_w\) is width of the grid, \(n\) is size of the environment, and \((X_O, Y_O)\) is the position of obstacle. \(R_G\) is the formula of the distance between the agent and the goal positions, \(R_O\) is the formula of the distance between the agent and the obstacle positions. Then \(R_G\) and \(R_O\) are summed up to become an environment matrix value.

\[
\begin{align*}
  l_I &= 1; \\
  l_J &= 1; \\
  k &= 1; \\
  n &= 100; \\
  \text{for } i &= k; i_I; n \\
  \text{for } j &= k; j_J; n \\
  R_o &= \left(\frac{j}{10} - Y_o\right)^2 + \left(\frac{i}{10} - X_o\right)^2; \\
  R_G &= \left(\frac{j}{10} - Y_G\right)^2 + \left(\frac{i}{10} - X_G\right)^2; \\
  A(i,j) &= \frac{1}{R_o} + R_o; \\
  \text{if } (A(i,j) > 300), A(i,j) = 300; \\
  \text{end} \\
  \text{end}
\end{align*}
\]

Figure 2. Source code program for environment map

2.2. Fuzzy Algorithm

Fuzzy algorithm was discovered by Zadeh in 1965 used for robot navigation path planning. Some researchers such as Vachtsevanos and Hexmoor [17] used it for a wheeled robot path planning. With this algorithm, the robot could avoid static obstacles. The other researcher, Surmann et al [18] also used fuzzy algorithm for mobile robot path planning. It was used for a path planning in an environment that has many obstacles.

In a robot path planning research, fuzzy algorithm has many weaknesses, so that the algorithm is combined with cell decomposition to find the fastest and shortest called FDT. The research of determining the shortest path using fuzzy decision tree has been carried out such as by Hamzei et al [19]. In his research, entitled Self-organizing Fuzzy decision tree for Robot Navigation: An On-line Learning Approach, they implemented this algorithm to search robot path and fuzzy rule base to detect obstacles.

Turnbull et al [20] also used fuzzy decision tree algorithm for path planning of UAV. This algorithm requires a lot of data used for training. The training enables UAV to move toward the goal position and avoid obstacles. This algorithm has a weakness that is it needs a long training process. Due to the weakness a new algorithm is developed with the principle of seeing close neighborhoods. Fuzzy decision tree algorithm with close neighbor’s optimum was developed by Lertworaprachaya [21].

Figure 3. The environment model
This paper describes fuzzy algorithms for path planning with grid values as the fuzzy input obtained from cell decomposition in a global path planning and the fuzzy output is motion direction of an agent that the design is shown in figure 3. It shows that the fuzzy has 5 inputs and 2 outputs in which the inputs are grid values located around the agent that is in the front, in 45 degree left, 45 degree right, left and right of the grids. While the output of the fuzzy is the value of direction for the x and y-axis.

Figure 4a shows member set which has a range of 0-300 and three members i.e. small (S), medium (M), and large (B) in which each has a range of [0 90] [90 210] and [210 300] respectively. The set of fuzzy output has a range of -1 to 1, which is shown in Figure 4b. It shows that the set of members for output have three members, namely the right (R), the center (Z), and Left (L) which each has of a range [-1 -0.4] [-0.4 0.4] and [0.4 1] respectively.

![Figure 4. Fuzzy input and output](image)

The fuzzy rule base is shown in figure 5. It is seen that there are two basic rules that is the basic rules of fuzzy X and for fuzzy Y. The basic rules of fuzzy X provides the value of direction for x-axis while the basic rules of fuzzy X provides the value of direction for x-axis. The value of direction of x and y axis move the agent towards the goal position and avoid obstacles. Variable A1 to A5 is a fuzzy input namely A1 is left input of the grids, A2 is 45 degree left, A3 is a front input, A4 is 45 degree right, and A5 is the right input of the grids.

```plaintext
if (A1<A2)&&(A1<A3)&&(A1<A4)&&(A1<A5)
    x = Negative;
    y = Zero;
else if (A2<A3)&&(A2<A4)&&(A2<A5)
    x = Negative;
    y = Positive;
else if (A3<A4)&&(A3<A5)
    x = Zero;
    y = Positive;
else if (A4<A5)
    x = Positive;
    y = Negative;
else
    x = Positive;
    y = Zero;
end
```

![Figure 5. The x and y rule based fuzzy](image)

### 2.3. Potential Field Algorithm

Potential field algorithm [22] is one of path planning algorithms which was developed by Khatib from the magnetic field. The equation of potential field algorithm is as follows:

$$ F = F_a + F_o $$  \hfill (1)
where $F_a$ and $F_r$ is the attraction and repulsion. Attractive force is the force that will cause the agent to move to the destination. The attractive force equation is as follows:

$$F_a(x) = -k(x - x_d)$$  \hspace{1cm} (2)

In which $k$ is the attractive potential field constant. The value of $k$ is $0 < k < 1$. $x$ shows the destination point of the agent and $x_d$ shows the coordinates of the agent.

The repulsion equation is as follows:

$$F_r(\rho) = \vartheta \left( \frac{1}{\rho} - \frac{1}{\rho_0} \right) \frac{1}{\rho^2} \frac{\partial \rho}{\partial x}$$  \hspace{1cm} (3)

In which $\vartheta$ is the repulsive potential field constant. The value of $\vartheta$ is $0 < \vartheta < 1$. $\rho$ shows the coordinates of the agent and $\rho_0$ shows the point of the obstacle. Many researchers have modified the potential field algorithm such as Rizqi et al [23] who has modified repulsive potential field. Ren et al [24] has modified potential field by using Newton's laws and applied it to mobile agents. Velagic et al [25] has modified the potential field in order to avoid local minima.

In this paper, the potential field algorithm was modified to provide weight for the value of environment matrices. To obtain the weight value, the Khatib’s equation of the attraction potential field was modified into the following:

$$F_{a,w}(x) = k \sqrt{(J - Y_o)^2 + (I - X_o)^2}$$  \hspace{1cm} (4)

In which $k$ is the attractive potential field constant. $(X_o, Y_o)$ shows the destination point of the agent and $(I, J)$ shows the coordinates of the agent.

While Khatib’s repulsion potential field equation was modified into the following:

$$F_{r,mn} = \frac{k_{rn}}{\sqrt{(J - Y_{on})^2 + (I - X_{on})^2}}$$  \hspace{1cm} (5)

In which $k_{rn}$ is the attractive potential field constant. $(X_{on}, Y_{on})$ shows the coordinates of the obstacle with $On$ is number of obstacle.

### 2.3. Environment Model Modified

This study explains fuzzy decision tree algorithm merged with cell decomposition algorithm for an agent path planning. The agent moves the goal position in an unknown environment. In the simulation, the merger of the two algorithms are unable to find the shortest path, therefore it is necessary to modify the method in order for the path planning to be optimal in finding the shortest path. The modification is conducted by adding potential field algorithm in the environment model with the source code program shown in figure 6.

![Figure 6. Source code program for environment map with modified potential field algorithm](image)
Figure 6 shows that $F_{x_d}$ is the attractive of potential fields as shown in equations 4 while $F_{x_o}$ is the repulsive of field potential as shown in equation 5. $K_A$ is the constant of the potential field attractive, and $K_R$ are the constant of the field potential repulsive. The sum of potential field force is used for the weight value of columns and rows in an environment matrix. If the sum of attractive and repulsive is a very large, then a limit value is given.

3. RESULTS AND ANALYSIS

The researchers used two softwares namely ROS (Robot Operating System) and Matlab. By using the matlab, the design and simulation for the Fuzzy decision tree Artificial Potential Fields (FDTAPF) algorithm could be created. Experiments were carried out with the design environment that was conducted by LIANG [29] with size of 100x100. Afterward, the environment Matrix derived from Liang’s was created to simulate the mobile robot. There were 2 experiments created ie in environments with multi obstacles and in environments with local minima.

![Figure 7. Experiment 1 in environment 1 with FDT and FDTAPF algorithm](image)

In experiment 1 in environment 1, the goal is to move the agent from the initial point to the destination point as shown in Figure 7 with FDT and FDTAPF algorithms. It shows that there is an environment that has six obstacles. The agent is placed in the position of (30, 95) denoted by green star. The agent moves towards the destination point (30, 10) denoted by blue star. In the figure it can be seen that there are two lines, namely red and blue. It is seen that the FDTAPF algorithm with red line is better than the FDT algorithm with blue line in term of that the red line has a shorter distance to reach the final destination.
In the following simulations, the initial and destination position point of the agent is changed as shown in Figure 8 with FDT and FDTAPF algorithms. In experiment 2 in the environment 1, the initial position of the agent is placed in (10, 10) denoted by green star and the destination point (90, 90) denoted by blue star. In the figure it can be seen that there are two lines, namely yellow and green. It is seen that the FDTAPF algorithm with yellow line is better than the FDT algorithm with green. By using FDTAPF algorithm, the agent can find the shortest path in both experiments in environment 1.

In the first experiment in environment 2, the goal is to move the agent from the initial point to the destination point as shown in Figure 9 with FDT and FDTAPF algorithms. It shows that there is an environment that has obstacles. The agent is placed in the position of (5, 5) denoted by green star. The agent moves towards the destination point (95, 95) denoted by blue star. From the figure that it can be seen that there are two lines, namely red and blue. From the figure it is seen that the FDTAPF algorithm with red line is better than the FDT algorithm with blue line in term of that the red line has shorter distance to reach the final destination.
Experiment 1 in environment 2 with FDT and FDTAPF algorithm can be analyzed by using contours as shown in Figure 10. In the figure, the contour difference between a weighted environment with a weightless environment is visible. By adding weights provided by potential algorithm, several contours exist in the environment which enable agent to find the shortest path. The starting point of the agent is shown in red color which has a high surface contour. While the destination point of the agent is shown in blue color which has low surface contour. Thus the agent will move to the goal from the higher contour towards the lower contour so that the path planning agents more optimal.

In the following simulations, the initial and destination position point of the agent is changed as shown in Figure 11 with FDT and FDTAPF algorithms. In experiment 2 in environment 2, the initial position point of the agent (45, 25) denoted by green star and the destination point (75, 80) denoted by blue star. From the figure that it can be seen that there are two lines, namely red and blue. From the figure it is seen that the FDTAPF algorithm with red line is better than the FDT algorithm with blue line in term of that the red line has shorter distance to reach the final destination. By using FDTAPF algorithm, the agent can find the shortest path in the environment 2.
Figure 12 shows that the agent path planning environment can be analyzed using contour. Figure A is path planning contour that do not use weight in the environment, while figure B is path planning contour which uses weights in the environment. The starting point of the agent is shown in red color which has a high surface contour. While the destination point of the agent is shown in blue color which has low surface contour. Thus the agent will move to the goal from the higher contour towards the lower contour so that the path planning agent is more optimal.

In experiment 3 in environment 2 shown in figure 13 the agent is in the environment with local minima. The agent stops if the agent cannot find the smallest weight. It can be overcome by using a potential field algorithm to obtain weight. In the figure it is seen that there are two color lines namely red and blue. It is seen that the FDTAPF algorithm with the red line is better than the FDT algorithm with the blue line. The agent in the blue line is not able to move and avoid local minima. While the agent in the red line is influenced by repulsion and attraction of potential field in that the agent is able to avoid local minima.

4. CONCLUSION
Fuzzy decision trees algorithm has been used in the previous researches to find a mobile agent path. By applying the algorithm, the agent is able to move to the destination point and detect multiple obstacles. When applied to an environment that has many obstacles, however, the algorithm is not able to avoid local minima.
minima. Therefore, this paper presents the modification of the FDT algorithm with potential field algorithm. Potential field algorithm provides weight to FDT algorithm. With the weight values provided by the potential field algorithm, the fuzzy decision tree algorithm is able to to find the shortest path and avoid local minima.

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