Branching Fraction Measurements of $B^+ \to \rho^+\gamma$, $B^0 \to \rho^0\gamma$, and $B^0 \to \omega\gamma$

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We present a study of the decays $B^+ \rightarrow \rho^+ \gamma$, $B^0 \rightarrow \rho^0 \gamma$, and $B^0 \rightarrow \omega \gamma$. The analysis is based on data containing 347 million $\bar{B}B$ events recorded with the BaBar detector at the PEP-II asymmetric $B$ factory. We measure the branching fractions $\mathcal{B}(B^+ \rightarrow \rho^+ \gamma) = (1.10^{+0.37}_{-0.33} \pm 0.09) \times 10^{-6}$ and $\mathcal{B}(B^0 \rightarrow \rho^0 \gamma) = (0.79^{+0.22}_{-0.20} \pm 0.06) \times 10^{-6}$, and set a 90% C.L. upper limit $\mathcal{B}(B^0 \rightarrow \omega \gamma) < 0.78 \times 10^{-6}$.

We also measure the isospin-averaged branching fraction $\mathcal{B}(B \rightarrow (\rho/\omega)\gamma) = (1.28^{+0.25}_{-0.24} \pm 0.09) \times 10^{-6}$, from which we determine $|V_{td}/V_{ts}| = 0.200^{+0.021}_{-0.020} \pm 0.015$, where the first uncertainty is experimental and the second is theoretical.

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In the Standard Model, the decays $B^+ \rightarrow \rho^+ \gamma$, $B^0 \rightarrow \rho^0 \gamma$, and $B^0 \rightarrow \omega \gamma$ arise mainly from $b \rightarrow d\gamma$ penguin diagrams containing a virtual top quark in the loop. By relating the three individual decay rates by isospin symmetry and using the measured ratio between the charged and neutral $B$ meson lifetimes $\tau_{B^+}/\tau_{B^0}$, an isospin-averaged branching fraction is defined: $\mathcal{B}(B \rightarrow (\rho/\omega)\gamma) = \frac{1}{2} \left[ \mathcal{B}(B^+ \rightarrow \rho^+ \gamma) + \frac{\tau_{B^0}}{\tau_{B^+}} \mathcal{B}(B^0 \rightarrow \rho^0 \gamma) + \mathcal{B}(B^0 \rightarrow \omega \gamma) \right]$. Recent calculations predict $\mathcal{B}(B \rightarrow (\rho/\omega)\gamma)$ to be in the range of $(0.9-1.8) \times 10^{-6}$ [2,3], where most of the uncertainty is due to the calculation of the form factor. These predictions could be modified by processes beyond the Standard Model [4].

While the exclusive decay rates have a large uncertainty due to non-perturbative long-distance QCD effects, much of this uncertainty cancels in the ratio of $\mathcal{B}(B \rightarrow (\rho/\omega)\gamma)$ to $B \rightarrow K^*\gamma$ branching fractions. Since the dominant diagram involves a virtual top quark, this ratio is related to the ratio of Cabibbo-Kobayashi-Maskawa (CKM) matrix elements $|V_{td}/V_{ts}|$ [2,3] via

$$\frac{\mathcal{B}(B \rightarrow (\rho/\omega)\gamma)}{\mathcal{B}(B \rightarrow K^*\gamma)} = \frac{|V_{td}/V_{ts}|^2}{\left(1 - m_{\rho}^2/M_B^2\right)} \frac{1}{\left(1 - m_{K^*}^2/M_B^2\right)} \zeta^2[1 + \Delta R].$$

(1)

The coefficient $\zeta$ is the ratio of the form factors for the decays $B \rightarrow \rho \gamma$ and $B \rightarrow K^*\gamma$ and $\Delta R$ accounts for different dynamics in the decay (e.g. annihilation diagrams can contribute to $B^+ \rightarrow \rho^+ \gamma$). Physics beyond the Standard Model could affect these decays, creating inconsistencies between the measurement of $|V_{td}/V_{ts}|$ obtained from this analysis and that obtained from the ratio of $B^0$ and $B^0_\tau$ mixing frequencies [6].

Previous searches by BaBar [7] and CLEO [8] found no evidence for the decays $B \rightarrow \rho \gamma$ and $B \rightarrow \omega \gamma$. An observation of the decay $B^0 \rightarrow \rho^0 \gamma$ was recently reported by the Belle collaboration [6]. This letter reports on a study of the decays $B^+ \rightarrow \rho^+ \gamma$, $B^0 \rightarrow \rho^0 \gamma$, and $B^0 \rightarrow \omega \gamma$ based on a data sample containing 347 million $\bar{B}B$ events, corresponding to an integrated luminosity of 316 fb$^{-1}$, collected with the BaBar detector [10] at the PEP-II asymmetric–energy $e^+e^-$ storage ring. These results supersede the previous BaBar measurements [7].

The decays $B \rightarrow \rho \gamma$ and $B \rightarrow \omega \gamma$ are reconstructed by combining a high-energy photon with a vector meson reconstructed in the decay modes $\rho^0 \rightarrow \pi^+\pi^- (B \sim 100\%)$, $\rho^+ \rightarrow \pi^+\pi^0 (B \sim 100\%)$, and $\omega \rightarrow \pi^+\pi^-\pi^0 (B = [89.1 \pm 0.7]%) [11].$

The dominant source of background is continuum events ($e^+e^- \rightarrow q\bar{q}$, with $q = u, d, s, c$) that contain a high-energy photon from $\pi^0$ or $\eta$ decays. Other backgrounds include photons from initial-state radiation (ISR) processes, decays of $B \rightarrow K^*\gamma$ ($K^* \rightarrow K\pi$), decays of $B \rightarrow (\rho/\omega)\pi^0$ or $B \rightarrow (\rho/\omega)\eta$ and combinatorial background from higher-multiplicity $b \rightarrow s\gamma$ decays. Selection requirements have been optimized for maximum statistical sensitivity with assumed signal branching fractions of $1.0 \times 10^{-6}$ and $0.5 \times 10^{-6}$ for the charged and neutral modes, respectively.

The photon from a signal $B$ decay is identified as a well-isolated energy deposit in the electromagnetic calorimeter with energy $1.5 < E_\gamma < 3.5$ GeV in the center of mass (CM) frame. The energy deposit must not be associated with any charged track and must meet several other requirements designed to eliminate background from hadronic showers and charged particles [12]. In order to veto photons from $\pi^0$ and $\eta$ decays, we associate each high-energy photon candidate $\gamma$ with each of the other photons $\gamma'$ in the event and reject candidates based on the value of the likelihood ratio

$$\frac{\mathcal{P}(m_{\gamma\gamma'}, E_{\gamma'}|i)}{\mathcal{P}(m_{\gamma\gamma'}, E_{\gamma}|\text{sig}) + \mathcal{P}(m_{\gamma\gamma'}, E_{\gamma'}|i)}$$

(2)

where $\mathcal{P}$ is the probability density function defined in terms of the invariant mass $m_{\gamma\gamma'}$ of the photon pair and the energy $E_{\gamma'}$ of $\gamma'$ in the laboratory frame, determined from simulated signal and background events. We also combine the high-energy photon candidate with photon conversions to $e^+e^-$ pairs, and reject the photon if the invariant mass is consistent with a $\pi^0$ or $\eta$.

Charged-pion candidates are selected from well-reconstructed tracks with a minimum momentum transverse to the beam direction of 100 MeV/c. A stringent $\pi^\pm$ selection algorithm [7] is applied to reduce background from charged kaons produced in $b \rightarrow s\gamma$ decays. The algorithm combines the information provided by the ring-imaging Cherenkov detector with the measurement of energy loss in the tracking system.

Photon candidates with energy greater than 50 MeV in the laboratory frame are combined into pairs to form $\pi^0$ candidates. For $B^0 \rightarrow \omega \gamma (B^+ \rightarrow \rho^+ \gamma)$ decays, the
invariant mass of the pair is required to satisfy \( 122 < m_{\gamma\gamma} < 150 \text{ MeV}/c^2 \) (\( 117 < m_{\gamma\gamma} < 148 \text{ MeV}/c^2 \)). We also require that the cosine of the opening angle between the daughter photons in the laboratory frame be greater than 0.413 (0.789).

The identified pions are combined into vector meson candidates by requiring \( 633 < m_{\pi^+\pi^-} < 957 \text{ MeV}/c^2 \), \( 636 < m_{\pi^+\pi^0} < 932 \text{ MeV}/c^2 \), and \( 764 < m_{\pi^+\pi^-\pi^0} < 795 \text{ MeV}/c^2 \) for \( p^0 \), \( p^+ \), and \( \omega \), respectively. The charged pion pairs must originate from a common vertex. The separation along the beam axis between this vertex and the one obtained by combining the other charged particles in the event is required to be less than 4 mm and to be measured with a precision better than 0.4 mm.

The photon and \( \rho/\omega \) candidates are combined to form the \( B \) meson candidates. We define \( \Delta E \equiv E_B^\ast - E_{\text{beam}} \), where \( E_B^\ast \) is the CM energy of the \( B \) meson candidate and \( E_{\text{beam}} \) is the CM beam energy. We also define the beam-energy-substituted mass \( m_{\text{ES}} \equiv \sqrt{E_{\text{beam}}^2 - p_B^2} \), where \( p_B^2 \) is the CM momentum of the \( B \) candidate. Signal events are expected to have a \( \Delta E \) distribution centered at zero with a resolution of about 50 MeV, and an \( m_{\text{ES}} \) distribution centered at the mass of the \( B \) meson, with a resolution of 3 MeV/c^2. We consider candidates in the ranges \(-0.3 < \Delta E < 0.3 \text{ GeV} \) and \( m_{\text{ES}} > 5.22 \text{ GeV}/c^2 \), which include sidebands that allow the combinatorial background yields to be extracted from a fit to the data.

To reject \( B \rightarrow \rho(\pi^0/\eta) \) and \( B \rightarrow \omega(\pi^0/\eta) \) events, we calculate the vector meson helicity angle, \( \theta_H \), defined in the \( \rho \) (\( \omega \)) rest frame as the angle between the \( \pi^- \) track (normal to the \( \omega \) decay plane) and the \( B \) momentum vector. We require \( |\cos\theta_H| < 0.75 \).

Contributions from continuum background processes are reduced by considering only events for which the ratio \( R_2 \) of second-to-zeroth Fox-Wolfram moments \( \left[ 16 \right] \) calculated using the momenta of all charged and neutral particles in the event is less than 0.7. A neural network combining the variables described below further suppresses continuum background. The quantity \( R_2 \), defined as \( R_2 \) in the frame recoiling against the photon momentum, is used to reject ISR events. To discriminate between the jet-like continuum background and the more spherically-symmetric signal events, we compute the angle between the photon and the thrust axis of the rest of the event (ROE) in the CM frame. The ROE is defined by all charged tracks and neutral energy deposits in the calorimeter that are not used to reconstruct the \( B \) candidate. We also calculate the moments \( L_i \equiv \sum_j p_j^i \cos\theta_j^i/\sum_j p_j^i \), where \( p_j^i \) and \( \theta_j^i \) are the momentum and angle with respect to an axis, respectively, for each particle \( j \) in the ROE. We use \( L_1 \), \( L_2 \), and \( L_3 \) with respect to the thrust axis of the ROE, as well as with respect to the photon direction. In addition, we calculate the \( B \) meson production angle \( \theta_B^\ast \) with respect to the beam axis in the CM frame. Differences in lepton and kaon production between background and \( B \) decays are exploited by using flavor-tagging variables \( \left[ 14 \right] \). The significance of the separation along the beam axis of the \( B \) meson candidate and ROE vertices is included as well. The purity of the selected sample is enhanced by a cut on the output of the neural network that retains 63%, 74%, and 71% of the signal events in the modes \( B^+ \rightarrow \rho^+\gamma \), \( B^0 \rightarrow \rho^0\gamma \), and \( B^0 \rightarrow \omega\gamma \), respectively.

The expected average candidate multiplicity in the selected signal events is 1.01 for \( B^0 \rightarrow \rho^0\gamma \) and 1.07 for both \( B^+ \rightarrow \rho^+\gamma \) and \( B^0 \rightarrow \omega\gamma \); in events with multiple candidates the one with the reconstructed vector meson mass closest to the nominal mass is retained. Applying all the selection criteria described above, we find efficiencies \( \left[ 15 \right] \) of 11.0% for \( B^+ \rightarrow \rho^+\gamma \), 14.1% for \( B^0 \rightarrow \rho^0\gamma \), and 7.9% for \( B^0 \rightarrow \omega\gamma \).

The signal content of the data is determined by a multidimensional unbinned maximum likelihood fit, which is constructed individually for each of the three signal decay modes. All fits use \( \Delta E \), \( m_{\text{ES}} \), \( \cos\theta_H \), and the neural network output \( N \). In order to facilitate the parametrization of the probability density function (PDF) used in the fit, the transformation \( \mathcal{NN} = \tanh^{-1}(c_1 \cdot N - c_2) \), in which the \( c_i \) are mode-dependent constants, is made. For decays \( B^0 \rightarrow \omega\gamma \) (\( \omega \rightarrow \pi^+\pi^-\pi^0 \)), the cosine of the angle between the \( \pi^+ \) and \( \pi^0 \) momenta in the \( \pi^+\pi^- \) rest frame (Dalitz angle) is added as a fifth observable.

In the fit we consider several hypotheses for the origin of the events: signal, continuum background, \( B \rightarrow K^*\gamma \) decays, and other \( B \) backgrounds. The likelihood function for a signal mode \( k \) (= \( \rho^+\gamma \), \( \rho^0\gamma \), \( \omega\gamma \)) is defined as

\[
\mathcal{L}_k = \exp \left( -\sum_{i=1}^{N_{\text{hyp}}} n_i \right) \left[ \frac{N_{\text{hyp}}}{\sum_{i=1}^{N_{\text{hyp}}} n_i} \prod_{i=1}^{N_{\text{hyp}}} n_i \mathcal{P}_i(\bar{x}_j; \bar{\alpha}_i) \right],
\]

where \( N_{\text{hyp}} \) is the number of event hypotheses, \( n_i \) is the yield of each hypothesis, and \( N_j \) is the number of candidate events observed in data. Since the correlations among the observables are found to be small in simulated event samples, we define the PDF \( \mathcal{P}_i(\bar{x}_j; \bar{\alpha}_i) \) for the \( i \)-th event hypothesis as the product of individual PDFs for each fit observable \( x_j \) given the set of parameters \( \bar{\alpha}_i \).

Each PDF is determined from a one-dimensional fit to a dedicated sample of simulated events. The \( \Delta E \) PDF is corrected for the observed difference between data and simulation by using samples of \( B \rightarrow K^*\gamma \) decays. All continuum background parameters float freely in the fits, while the shapes of the signal and \( B \) background distributions are fixed according to the Monte Carlo simulation. The signal \( m_{\text{ES}} \) spectra are described by Crystal Ball functions \( \left[ 10 \right] \), the angular distributions are modeled by polynomials, and the distributions of \( \Delta E \) and \( \mathcal{NN} \) are parametrized as \( f(x) = \exp \left( \frac{-i(x-\mu)^2}{2\sigma_{L,R}^2} \right) \), where \( \mu \) is the peak position of the distribution, \( \sigma_{L,R} \) are the widths on the left and right of the peak, and \( \alpha_{L,R} \) are a measure of the tails on the left and right of the peak, re-
signal reconstruction efficiency and the modeling of signal.

The latter contributes to the uncertainties on the signal
yields. The systematic error affecting the signal efficien-
cy includes uncertainties on tracking, particle identifi-
cation, γ and π0 reconstruction, π0/η veto and the
neural network selection. These uncertainties are deter-
mined from independent data control samples. To es-
imate the uncertainty related to the modeling of the sig-
nal and B background in the Monte Carlo, we vary the paa-
arameters of the PDFs that are fixed in the fit within
their errors. The uncertainty related to the choice of a
specific functional form for the shape of the NN distri-
bution is evaluated by using a binned PDF as an alterna-
tive description. All relative and absolute normalizations
of B background components that are fixed in the fit are
varied within their errors. For all these variations, the
corresponding change in the fitted signal yield is taken
as a systematic uncertainty.

The branching fractions are calculated from the mea-
sured signal yields assuming $B(\Upsilon(4S) \to B^+\bar{B}^0) =
B(\Upsilon(4S) \to B^+B^-) = 0.5$. The results are listed in Ta-
ble I. For $B^0 \to \omega\gamma$, we also compute the 90% con-
fidence level (C.L.) upper limit $B(B^0 \to \omega\gamma) < 0.78 \times 10^{-6}$ using
a Bayesian technique. We determine the branching frac-
tion upper limit $\mathcal{B}_{\text{fit}}$ such that $\int_0^\infty \mathcal{L} \, d\mathcal{B} / \int_0^\infty \mathcal{L} \, d\mathcal{B} = 0.90,$
\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
\textbf{Mode} & $n_{\text{sig}}$ & $\Sigma$ & $\sigma$ & $B(10^{-6})$ \\
\hline
$B^+ \to \rho^+\gamma$ & 42.0^{+14.0}_{-12.7} & 3.8σ & 11.0 & 1.10^{+0.37}_{-0.33} \pm 0.09 \\
$B^0 \to \rho^0\gamma$ & 38.7^{+10.6}_{-9.8} & 4.9σ & 14.1 & 0.79^{+0.22}_{-0.20} \pm 0.06 \\
$B^0 \to \omega\gamma$ & 11.0^{+6.7}_{-5.6} & 2.2σ & 7.9 & 0.40^{+0.24}_{-0.20} \pm 0.05 \\
\hline
$B \to (\rho/\omega)\gamma$ & 6.4σ & & & 1.25^{+0.25}_{-0.24} \pm 0.09 \\
$B \to \rho\gamma$ & 6.0σ & & & 1.36^{+0.29}_{-0.37} \pm 0.10 \\
\hline
\end{tabular}
\caption{The signal yield ($n_{\text{sig}}$), significance ($\Sigma$) in stan-
dard deviations including systematic errors, efficiency ($\sigma$), and
branching fraction ($B$) for each mode. The errors on $n_{\text{sig}}$ are
statistical only, while for the branching fraction the first error
is statistical and the second systematic.}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline
\textbf{Source of error} & $\rho^+\gamma$ & $\rho^0\gamma$ & $\omega\gamma$ & $\rho\gamma$ & ($\rho/\omega)\gamma$ \\
\hline
Tracking efficiency & 1.0 & 2.0 & 2.0 & 1.4 & 1.5 \\
Particle identification & 2.0 & 4.0 & 2.0 & 2.9 & 2.7 \\
Photon selection & 1.9 & 2.6 & 1.7 & 2.2 & 2.1 \\
$\pi^0$ reconstruction & 3.0 & - & 3.0 & 1.9 & 2.5 \\
$\pi^0$ and $\eta$ veto & 2.8 & 2.8 & 2.8 & 2.8 & 2.8 \\
$NN$ efficiency & 1.0 & 1.0 & 1.0 & 1.0 & 1.0 \\
$NN$ shape & 0.4 & 0.3 & 2.3 & 0.4 & 0.7 \\
Signal PDF shapes & 4.8 & 3.3 & 2.4 & 3.1 & 2.6 \\
$B$ background PDFs & 3.9 & 2.9 & 9.7 & 3.2 & 3.1 \\
$\bb$ sample size & 1.1 & 1.1 & 1.1 & 1.1 & 1.1 \\
$B(\omega \to \pi^+\pi^-\pi^0)$ & - & - & 0.8 & 0.8 & 0.1 \\
\hline
Sum in quadrature & 8.1 & 7.4 & 11.6 & 7.0 & 6.9 \\
\hline
\end{tabular}
\caption{Fractional systematic errors (in %) of the mea-
sured branching fractions.}
\end{table}
assuming a flat prior in the branching fraction and taking into account the systematic uncertainty.

We test the hypothesis of isospin symmetry by measuring the quantity \( \Gamma(B^+ \to \rho^+ \gamma)/[2\Gamma(B^0 \to \rho^0 \gamma)] - 1 = -0.35 \pm 0.27 \). The result is consistent with the theoretical expectation [2].

The isospin-averaged branching fraction is extracted from a simultaneous fit to the three decay modes:

\[
\mathcal{B}(B \to (\rho/\omega)\gamma) = (1.25^{+0.35}_{-0.24} \pm 0.09) \times 10^{-6}.
\]

This result is used to calculate the ratio \( |V_{td}/V_{ts}| \) by means of Eq. (5). Following [17], we obtain

\[
|V_{td}/V_{ts}| = 0.200^{+0.021}_{-0.020} \pm 0.015,
\]

where the first error is experimental and the second is theoretical. This result is consistent with the measurement of this ratio from the study of \( B^0 \) and \( B^0_s \) mixing [3].

In conclusion, we have measured the branching fractions of \( \mathcal{B}(B^+ \to \rho^+ \gamma) = (1.10^{+0.37}_{-0.33} \pm 0.09) \times 10^{-6} \) and \( \mathcal{B}(B^0 \to \rho^0 \gamma) = (0.79^{+0.22}_{-0.20} \pm 0.06) \times 10^{-6} \), where the first error is statistical and the second is systematic. These are the most precise measurements of these branching fractions to date. We have also set a 90\% C.L. upper limit on the \( B^0 \to \omega\gamma \) branching fraction of \( \mathcal{B}(B^0 \to \omega\gamma) < 0.78 \times 10^{-6} \). From the isospin-averaged branching fraction \( \mathcal{B}(B \to (\rho/\omega)\gamma) = (1.25^{+0.35}_{-0.24} \pm 0.09) \times 10^{-6} \), we determine \( |V_{td}/V_{ts}| = 0.200^{+0.021}_{-0.020} \pm 0.015 \).

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