An Observationally Constrained Model of a Flux Rope that Formed in the Solar Corona

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Abstract

Coronal mass ejections (CMEs) are large-scale eruptions of plasma from the coronae of stars. Understanding the plasma processes involved in CME initiation has applications for space weather forecasting and laboratory plasma experiments. James et al. used extreme-ultraviolet (EUV) observations to conclude that a magnetic flux rope formed in the solar corona above NOAA Active Region 11504 before it erupted on 2012 June 14 (SOL2012-06-14). In this work, we use data from the Solar Dynamics Observatory (SDO) to model the coronal magnetic field of the active region one hour prior to eruption using a nonlinear force-free field extrapolation, and find a flux rope reaching a maximum height of 150 Mm above the photosphere. Estimations of the average twist of the strongly asymmetric extrapolated flux rope are between 1.35 and 1.88 turns, depending on the choice of axis, although the erupting structure was not observed to kink. The decay index near the apex of the axis of the extrapolated flux rope is comparable to typical critical values required for the onset of the torus instability, so we suggest that the torus instability drove the eruption.

Key words: Sun: corona – Sun: coronal mass ejections (CMEs) – Sun: magnetic fields

1. Introduction

Coronal mass ejections (CMEs) are large-scale eruptions of plasma from the coronae of stars, and there is currently no consensus regarding their cause. Understanding the stability of the plasma structures involved in CME initiation is important for forecasting space weather sufficiently far in advance of CME arrival at Earth.

Solar CMEs have large kinetic energies (~10^{32} erg; Forbes 2000), so many CME models describe processes by which an increasing amount of energy is stored in the corona and then suddenly released (Forbes 2000). The question of what processes cause this storage and release of energy in CMEs is closely tied to understanding the pre-eruptive configuration of the corona, because certain eruption mechanisms may only be relevant to specific topologies. Measurements taken at 1 au have in some cases revealed that CMEs arriving at Earth contain twisted magnetic structures called flux ropes (Burlaga et al. 1981), however it is debated whether these flux ropes form before or after CME onset (Antiochos et al. 1999; Moore et al. 2001; Green & Kliem 2009).

There are a wide range of proposed CME triggers that bring the coronal magnetic field to the brink of eruption, including rotation of sunspot fragments around each other (e.g., Yan et al. 2012; James et al. 2017), magnetic reconnection (e.g., flux cancellation; van Ballegooijen & Martens 1989, and tether-cutting; Moore et al. 2001), and the helical kink instability of a flux rope (Török & Kliem 2005), but there are only two main groups of theories regarding the process that drives the rapid expansion of CMEs. One group assumes that CMEs are driven by an ideal magnetohydrodynamic instability involving a flux rope, such as the torus instability (van Tend & Kuperus 1978; Kliem & Török 2006; Démoulin & Aulanier 2010), whereas the other set of theories assumes that CMEs are driven by flare reconnection (Antiochos et al. 1999; Temmer et al. 2010; Karpen et al. 2012).

James et al. (2017; hereafter Paper I) observationally studied the pre-eruptive configuration of a CME that occurred on 2012 June 14. The CME originated from NOAA Active Region 11504 when it was near the center of the solar disk. Extreme-ultraviolet (EUV) images show a transient sigmoid during a confined flare two hours before the CME, suggesting that a flux rope was present before the onset of eruption, and the flux rope footpoints were inferred by EUV dimmings and flare ribbons. For details on observational signatures of flux ropes, see Paper I and references within. Observations from a number of EUV channels suggest that the flux rope formed by reconnection in the corona rather than in the photosphere or chromosphere, which is confirmed by the measured coronal plasma composition in the flux rope. For more examples of flux ropes formed via coronal reconnection, see Patsourakos et al. (2013) and Nindos et al. (2015).

The conclusions of Paper I were based on indirect indications of the flux rope, because presently we are unable to directly measure the coronal magnetic field. However, techniques have been developed to extrapolate the coronal magnetic field from complex (but routinely available) photospheric measurements under the assumption that the corona is in a force-free state (Wiegelmann & Sakurai 2012), i.e.,

$$J \times B = 0,$$
where \( \mathbf{B} \) is the magnetic field vector and \( \mathbf{J} \) is the electric current density

\[
\mathbf{J} = \frac{1}{\mu_0} \nabla \times \mathbf{B}.
\]

This assumption is satisfied by either a potential field \((\mathbf{J} = 0)\), or a field in which electric currents are parallel to the magnetic field vector \((\nabla \times \mathbf{B} = \alpha \mathbf{B})\). In the nonlinear case, the force-free parameter, \( \alpha \), varies for different field lines. The nonlinear force-free field (NLFFF) approximation is the simplest method that can reproduce the electric currents and complex distributions of twist associated with a flux rope embedded in an arcade.

In this work, we use an NLFFF extrapolation to test the hypothesis of Paper I, that a flux rope formed before the CME that occurred at \( \approx 13:30 \) UT on 2012 June 14, and investigate the cause of its eruption.

2. Data, Method, and Validation of the Model

The NLFFF extrapolation of NOAA Active Region 11504 was performed using a photospheric magnetogram produced by the Helioseismic and Magnetic Imager (HMI; Scherrer et al. 2012) on board the Solar Dynamics Observatory (SDO; Pesnell et al. 2012). The chosen magnetogram was taken at \( \approx 12:24 \) UT on 2012 June 14; approximately one hour after the first observational indication that a flux rope was present, and one hour before the CME began (see Paper I).

The observed EUV sigmoid extended to the south of the NOAA Active Region 11504 before the CME occurred (see Figure 5(c) of Paper I), and so the field-of-view of the publicly available HMI SHARP series magnetogram (Bobra et al. 2014) was too small to accurately reproduce the sigmoidal field in the extrapolation. A bespoke SHARP-style magnetogram was produced with a large enough field-of-view to accommodate the size of the sigmoid \((\approx 400'' \times 600'')\), while still excluding as much of the dispersed negative magnetic flux to the south of the active region as possible (see the red boxes in Figure 1).

The magnetogram was re-binned to 1/6 resolution, such that each pixel in the cylindrical equal-area projection represents an angular diameter of \(0.18''\) (equivalent to \(3''\) or \(\approx 2.18 \) Mm at disk center when viewed from 1 au) and smoothed using the median of a 7-pixel boxcar. To alleviate the impact on the extrapolated field caused by the isolated negative magnetic flux to the south of the active region, a balance of positive and negative magnetic flux was enforced over the magnetogram corresponding to an increase of \(5.2\) G in each pixel (which is far smaller than the \(100\) G error estimation suggested by Hoeksema et al. (2014) and corresponds to a total change of \(13.6\)\% in the open field flux). The magnetogram was then pre-processed using the method of Fuhrmann et al. (2007) to reduce the total Lorentz force by applying variations to the horizontal and vertical magnetic field components. Modifications to the observed horizontal (vertical) field component in each pixel were limited to \(80\) G or \(30\)\% (\(30\) G or \(10\)\%) of its initial value—whichever is largest.

The coronal magnetic field was then extrapolated from the pre-processed magnetogram using the magneto-frictional NLFFF method detailed by Valori et al. (2010), yielding a model of the active region with a force-free parameter \(\sigma_J \approx 25\%\) (Wheatland et al. 2000) and solenoidal error limited to \(9\%\) of the total energy (Valori et al. 2013). The top boundary of the extrapolation volume was chosen to sufficiently accommodate the height of a toroidal flux rope with a footpoint separation as indicated in Figure 6 of Paper I.

To check the validity of the extrapolation, we compare the extrapolated magnetic field to EUV observations of the active region produced by the Atmospheric Imaging Assembly (AIA; Lemen et al. 2012) on board SDO after re-projecting the NLFFF extrapolated field lines onto the AIA plane-of-sky images (as in Polito et al. 2017). Figure 2 shows that the extrapolation reproduces the large-scale active region emission.
structures seen in the 193 Å channel of AIA, including field lines that fan out from the edges of the active region and a sheared arcade in the core of the active region (shown by the southern group of white field lines in Figure 2(a)) that matches the observed sheared arcade (see Section 3.3 and Figure 5 of Paper I for more details).

3. The Pre-eruptive Flux Rope

We use the force-free parameter, \( \alpha \), as a proxy for twist in the extrapolated magnetic field. Figure 3(a) shows a volume between the active region sunspots in the NLFFF model, where \( \alpha \) is large relative to the rest of the extrapolated field (see Figure 3(a)). Visualizing magnetic field lines that pass through this region where \( \alpha > 0.02 \text{ Mm}^{-1} \) reveals a flux rope (see Figures 3(b) and (c)). The location and shape of the flux rope remarkably matches most, if not all, of the observational constraints identified in Section 4 of Paper I.

The flux rope extends high in the corona, with its highest point reaching \( \approx 150 \text{ Mm} (\approx 0.2 R_\odot) \) above the photosphere. The axis of the flux rope is not planar, but is oriented roughly eastward and inclined to the south with respect to the vertical. The flux rope is highly asymmetric and has a strongly inhomogeneous distribution of right-handed twist. The flux rope cross-section shown in Figure 3(a) has a major diameter of \( \approx 105 \text{ Mm} \) and a minor diameter of \( \approx 35 \text{ Mm} \).

The footpoints of the extrapolated flux rope are located in the north-western penumbra of the positive sunspot and to the south of the negative sunspot. EUV observations, however, suggest that the western footpoint of the flux rope was rooted in the south-western penumbra of the positive sunspot during the eruption (see Figure 6 of Paper I). This difference of approximately half the sunspot diameter could be due to modification of the magnetogram induced by pre-processing, to the difference in time between the pre-eruptive extrapolation and observations during the dynamic phase of the eruption, or to projection effects in the coronal EUV data.
In addition to the set of observations presented in Paper I, a differential emission measure (DEM) inversion was performed using the method of Cheung et al. (2015) to study the thermal emission of the active region. At the time of the extrapolation, the sigmoid and underlying flare arcade observed in the EUV range emitted most strongly in the temperature range $\log(T/K) = 6.85$–7.15. This is consistent with their observation in the 131 Å channel of AIA, which has a peak in temperature response at 11 MK (Lemen et al. 2012), and confirms flux rope temperatures from previous DEM studies (e.g., Cheng et al. 2012). The shape of the sigmoid in the EUV observations and DEM closely matches extrapolated field lines that pass through the strong region of current density in the bottom-third of the flux rope (see Figure 4).

Field lines that reproduce the observed sheared arcade were also found to pass through a region of strong current beneath the flux rope (see the green field lines in Figures 4(c) and (d); the average value of $\alpha$ here is $\approx 0.07$ Mm$^{-1}$). In addition to the many observational details summarized above, the similarly hot temperatures and high current densities of the sigmoid and the arcade support the hypothesis of Paper I that the flux rope and flare arcade form as the products of magnetic reconnection in the corona.

The flux rope (as defined by the region of large $\alpha$ in the red box in Figure 3(a)) contains $4 \times 10^{20}$ Mx of magnetic flux ($\approx 3\%$ of half the unsigned active-region flux). The average value of $\alpha$ in the flux rope is $\approx 0.07$ Mm$^{-1}$, as in the part of the sheared arcade where the current density is stronger. The total electric current within the flux rope is $2.3 \times 10^{11}$ A, with an average current density of $9.9 \times 10^{-5}$ A m$^{-2}$. These values are similar in magnitude to previous estimations of currents in prominences (Filippov et al. 2015, and references within).

### 3.1. Twist and Writhe

The flux rope is twisted and extends very high in the atmosphere, so we investigate whether it is actually stable. According to the test in Section 4.3 of Valori et al. (2010), an
unstable equilibrium would result in an uncommonly long computational time, which was not recorded in this case.

The helical kink instability will occur if the flux rope twist exceeds a critical value. To quantify the twist in our very asymmetric case, the twist of individual field lines in the flux rope was calculated around an axis, and the average was taken (Guo et al. 2010, 2013). Following Guo et al. (2017), the axial field line is defined as the field line with the smallest ratio of tangential-to-normal magnetic field components with respect to a plane roughly perpendicular to the body of the flux rope.

Given the marked asymmetry of the flux rope, we took three slices through the flux rope with different inclinations, resulting in three axes and therefore three values of the average twist, namely 1.35, 1.61, and 1.88 turns. The axes are similar in height and length (for reference, the first axis is ≈350 Mm long and reaches up to ≈120 Mm above the photosphere). The same set of flux rope field lines were used to determine the twist around each of the three axes.

Török & Kliem (2003) examined a Titov & Démoulin (1999) flux rope topology and found a critical twist of $3.7\pi$ (1.75 turns) for the onset of the helical kink instability. This twist threshold is comparable to two of the values obtained for the asymmetric, non-uniform flux rope in this work.

The observations detailed in Paper I show no significant sign of the flux rope kinking before or during the eruption. In fact, the axis of the flux rope changed so little that the CME configuration measured in situ closely matched the pre-eruptive configuration (Palmerio et al. 2017). Therefore, we suggest that the critical twist required for this flux rope to become kink unstable was not reached.

The writhe of the three axes were 0.29, 0.09, and −0.07 turns. The axis that resulted in the largest value of average twist was the one with the smallest writhe, and vice versa. Therefore, the sum of the twist and writhe is closer to being independent of the choice of the plane used to determine the axis (as expected; Török et al. 2010).

Guo et al. (2017) concluded that a good proxy of the magnetic helicity in the current-carrying field inside a finite volume is

$$H_{TW} = \Phi^2 (\text{Twist} + \text{Writhe}),$$

where $\Phi$ is magnetic flux. In our case, using the total magnetic flux in the flux rope, this method gives a maximum helicity estimate of $3 \times 10^{41}$ Mx$^2$. On the other hand, using the extrapolated field, the helicity of the closed, current-carrying field, $H_p$, in the extrapolation volume is $4 \times 10^{42}$ Mx$^2$, which is 14 times larger than $H_{TW}$. Part of this discrepancy may originate from underestimating the magnetic flux in the flux rope when defining the boundary of the flux rope using the force-free parameter, $a$. However, because $H_{TW}$ scales with $\Phi^2$, there would need to be a factor of $\sqrt{14} \approx 3.7$ error in the magnetic flux to fully explain the difference.

The mutual helicity between the potential field and current-carrying field, $H_{pj}$ (as defined, e.g., by Equation (11) in Pariat et al. 2017), $\approx 1 \times 10^{39}$ Mx$^2$. The total helicity in the extrapolation volume is then given by $H = H_j + 2H_{pj} \approx 2.4 \times 10^{39}$ Mx$^2$. We are able to provide the first estimation of the eruptivity proxy recently introduced by Pariat et al. (2017) for an NLFFF extrapolation of an active region, equal to $H_j/H = 0.17$.

### 3.2. Decay Index

A toroidal magnetic structure, such as a flux rope, may be unstable to perturbations if the overlying magnetic field strength decreases too rapidly with height. This phenomenon is referred to as the torus instability (Kliem & Török 2006). The rate of change of magnetic field strength with height may be quantified by the decay index, $n$, defined as

$$n = -\frac{d \ln B_{ext,p}}{d \ln R},$$

where $B_{ext,p}$ is the strength of the poloidal component of the magnetic field external to the flux rope (non-current-carrying), and $R$ is the major radius of the torus.

In order to estimate the decay index at the height of the flux rope, we perform a potential field extrapolation using the method of Alissandrakis (1981) to approximate magnetic field external to the flux rope, and take the poloidal component as perpendicular to the central section of the flux-rope axis. We compute the decay index using the gradient of the poloidal field component in two planes inclined parallel with, and perpendicular to, the axis of the flux rope (see Figure 5).

The decay index near the center (axis apex) of the extrapolated flux rope is equal to 1.8 (2.0). The value of the critical decay index required for the torus instability of a symmetric torus with a large aspect ratio is 3/2 (Bateman 1978; Kliem & Török 2006), and a number of studies have found similar values in magnetohydrodynamic simulations (Török & Kliem 2007; Aulanier et al. 2010; Kliem et al. 2013; Zuccarello et al. 2015, 2016). However, some studies have also found lower and higher critical decay indices (e.g., $n_{\text{crit}} = 1.1–1.3$; Démoulin & Aulanier 2010, and $n_{\text{crit}} \approx 2$; Fan 2010). The extrapolated asymmetric flux rope lays in the upper range of the known stability limit for the torus instability, which is compatible with the eruption of the flux rope occurring one hour later.

### 4. Conclusions

In this study, we test the hypothesis of James et al. (2017; Paper I) that a magnetic flux rope formed in the corona of NOAA Active Region 11504 before erupting as a CME. We produce an NLFFF extrapolation of the coronal magnetic field from a photospheric magnetogram one hour before the onset of eruption that closely supports the observational conclusions of Paper I.

The axis of the extrapolated flux rope reaches $\approx 120$ Mm above the photosphere ($\approx 150$ Mm at the top of the flux rope). The decay index near the center of the flux rope is $\approx 1.8$, which is comparable to the critical value for the torus instability onset determined in other works. Therefore, we argue that the torus instability drove the eruption.

The extrapolation represents the coronal magnetic field one hour before the eruption. During that hour, it is likely that a triggering process further evolved the field (for reference, the coronal transit time in our model is about 140 s). Vemareddy et al. (2017) observed the eruption of a highly twisted prominence (flux rope; 2.96 turns), and concluded that the helical kink instability caused the system to rise to the point at which the torus instability set in. Our flux rope has an average twist in the range of 1.35–1.88 turns, and although this is similar to estimates of the critical twist for the kink instability to occur, the observations presented in Paper I suggest that
kinking did not occur. However, the flux rope in this study forms already high in the corona and does not need to be raised by another mechanism. Instead, the motion of umbral sunspot fragments around each other may have inflamed and therefore weakened overlying field, leading to the torus instability. Our NLFFF extrapolation closely matches this scenario proposed in Paper I, and therefore further supports the proposal that the eruption was triggered by photospheric flows and driven by the torus instability.

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Figure 5. The decay index is computed in slices along and perpendicular to the flux rope axis. The decay index at the center of the flux rope is \( \approx 1.8 \).
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