Comparative Study Between Fuzzy and Sliding Mode Control Based on a BDFIG

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Abstract – Brushless doubly fed induction (BDFIG) is one of the best solutions of the previous research efforts about wind-power converter, which is represented by the absence of a brush gear and less maintenance cost, especially in the harsh regions. This task presents a comparative evaluation between a sliding mode and Fuzzy control. It demonstrates also the robustness of these two regulators against supply voltage and load disturbances. Furthermore, we have shown the undesirable phenomenon of oscillations having a finite frequency and amplitude, which is known as ‘chattering’ resulted from a sliding mode control which is based on Lyapunov approach theorem. The control of the system and BDFIG are both integrated in variable speed wind energy conversion. The performances of these control systems have been tested and analyzed in Matlab Simulink.

Keywords: Brushless doubly-fed induction generator, Neuro-Fuzzy Sliding mode control

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NOMENCLATURE

Wind Turbine

\[ V_q^s, V_d^s, V_q^r, V_d^r, I_q^s, I_d^s, I_q^r, I_d^r, \psi_q^s, \psi_d^s, \psi_q^r, \psi_d^r, R_p, R_w \]  Stator and rotor d-q reference frame voltages

\[ R_{en} \]  Rotor winding resistances

\[ P_p \]  Total cyclic stators inductances

\[ Q_p \]  Number of pole pairs for power control

\[ L_r \]  Total cyclic rotor inductance

\[ L_{mp}, L_{nc} \]  Magnetizing inductances

\[ w_c, w_p, w_n \]  Stators synchronous angular frequency

\[ R_c \]  Number of pole pairs for power control

\[ L_{mp}, L_{nc} \]  Electromagnetic torque

\[ p_c \]  Active of stator powers

\[ p_r \]  Reactive of stator powers

Abbreviations

DFIG  Doubly fed induction
BDFIG  Brushless Doubly Fed Induction Generator
DFIG  Doubly Fed Induction Generator
BDFIG  Doubly Fed Induction Generator
ANN  Artifical neural network
SMC  Sliding mode Control
NF - SMC  Neuro Fuzzy Sliding mode Control
I. Introduction

During the last years, there was a considerable exploitation of wind power energy which was expected to supply 5% of electrical global power during 2016, it suggests an approximation of 25% by the end of 2020 [1].

Undoubtedly, the doubly fed induction (DFIG) has become the most useful model in wind power application. But because of the presence of slip ring and brushes which requires more control and maintenance; therefore, it limits its application in harsh environment [2,3]. In this way, the emerging of BFIG has made up for many drawbacks of usual electric machines, as being Brushless and without slip ring.

Brushless doubly fed induction generator (BDFIG) includes a stator which incorporates two sets of three phase winding with different number of poles. The first is connected directly to the electrical grid, named the power winding (PW). The second is laid through a bi-directional converter to the grid, called control winding (CW)[3,4].

The rotor of BDFIG consists of specially designed nested loops which may be connected or separated from each other as presented in the following figure 1.

The Fuzzy logic control has been considered as one of the most successful expert systems which has been widely applied in control applications. [5]. As it doesn’t require a detailed mathematical model, it just uses the knowledge of the total operation of the system to build its based rule.

The Sliding mode control strategy is determined by the sum of two control laws: switching and equivalent It requires a detailed mathematical model, it just uses the discontinuous control action [8]. Signal across the sliding surface, satisfying the sliding condition. Nevertheless, this type of control has law [6,7].

II. Modeling of the Brushless Doubly Fed Induction Generator

The general relationships between these amounts as well as the electrical speed of the rotor for the 50 Hz system is

\[
\begin{align*}
\omega_p &= 2\pi 50 \\
\omega_r &= \omega_p - \omega_n p_p \\
\omega_e &= \omega_p - (p_p + p_c)\omega_n
\end{align*}
\]

(1)

The expressions for states' and rotor flux connections are given by the following equation:

\[
\begin{align*}
\psi_{q_p} &= L_{q_p}I_{q_p} + L_{mp}I_{q_r} \\
\psi_{d_p} &= L_{d_p}I_{d_p} + L_{mp}I_{d_r} \\
\psi_{q_r} &= L_{mp}I_{q_p} + I_{r} + L_{mc}I_{q_c} \\
\psi_{d_r} &= L_{mp}I_{d_p} + I_{r} + L_{mc}I_{d_c} \\
\psi_{q_c} &= L_{sc}I_{q_p} + L_{mc}I_{q_r} \\
\psi_{d_c} &= L_{sc}I_{d_p} + L_{mc}I_{d_r}
\end{align*}
\]

(2)

Electromagnetic Torque of the wind turbine is given as:

\[
c_t = \frac{1}{2} \left(R_1 (\psi_{q_p} I_{d_p} - \psi_{d_p} I_{q_p}) + B_L m \left(\psi_{q_p}^2 - \psi_{d_p}^2\right)\right)
\]

(3)

III. Field Oriented Control of BDFIG

The surface orientation power machine has been selected so as to obtain a good decoupled control. [4]

\[
\begin{align*}
\psi_{q_p} &= \psi_{d_p} &= 0.
\end{align*}
\]

The obtained control strategy for the BDFIM resembles to the well-known stator field orientation control used in the (BDFIM).

By neglecting resistances of the stator phases the stator voltage will be expressed by:

\[
\begin{align*}
\psi_{q_p} &= 0 \\
\psi_{d_p} &= \psi_{d_p}
\end{align*}
\]

(4)

The stator active and reactive power can be written according to the stator currents as:

\[
\begin{align*}
\left\{\begin{array}{l}
P_s = \psi_{q_p}U_{q_p} - \psi_{d_p}U_{d_p} + 4d\psi_{q_p} - \psi_{q_p}d

\end{array}\right.
\end{align*}
\]

(5)

The stator active and reactive power and voltages are given by:

\[
\begin{align*}
\psi_{q_p} &= R_s I_{q_p} + \frac{4}{s^2} (\psi_{q_p} I_{d_p} + \psi_{d_p} I_{q_p}) + \psi_{q_p} (\psi_{q_p} I_{d_q} + \psi_{d_q} I_{q_p} - \psi_{q_q} I_{d_q}) \\
\psi_{d_p} &= R_s I_{d_p} + \frac{4}{s^2} (\psi_{q_p} I_{d_p} + \psi_{d_p} I_{q_p}) - \psi_{q_p} (\psi_{q_q} I_{d_q} + \psi_{d_q} I_{q_p} - \psi_{q_q} I_{d_q})
\end{align*}
\]

(6)
Where:

\[
\delta_1 = \frac{l_{\text{ref}} - l_{\text{mp}}}{l_{\text{mp}}}, \quad \delta_2 = \frac{l_{\text{ref}} + l_{\text{mp}}}{l_{\text{mp}}}, \quad \delta_3 = l_{\text{ref}} - \frac{l_{\text{ref}}}{l_{\text{mp}}}, \quad \delta_4 = \frac{l_{\text{ref}}}{l_{\text{mp}}} - \frac{l_{\text{ref}}}{l_{\text{mp}}}
\]

(7)

The block-diagram representing the internal model of the system is presented in Figure 2. The input blocks relating \(v_1\), \(v_2\) represent the simplified stator converter model. Knowing equations (5) and (6), it is then possible to synthesize the regulators.

### III.1 Fuzzy Control

Fuzzy controllers are non-conventional linear controllers. They can give satisfactory results if they are built correctly using the schema of the system operator. Their design is composed of: (1) determining the inputs, (2) establishing rules and (3) the method of calculation to convert the rules in a net output signal, known defuzzification. First of all, the input index in this case is the error and the variance ratio. The error index is estimated and based on the net value the signal; it can be expressed in terms of degree of composition of fuzzy sets. The shape of fuzzy sets can be determined by the expert knowledge of the system. The following step is to build the fuzzy rules, again based on the expert knowledge of control problems, to accommodate all possible combinations of memberships.

| E/\Delta e | BN | SN | AZ | SP | BP |
|-----------|----|----|----|----|----|
| BN        | BN | BN | BN | SP | AZ |
| SN        | SN | SN | SN | AZ | SP |
| AZ        | SN | SN | AZ | SP | SP |
| SP        | SN | AZ | SP | SP | BP |
| BP        | AZ | SP | BP | BP | BP |
III.2. Sliding Mode Control

In order to improve and enhance the response of our system; we add another loop sliding mode. This type of control appeared for the first time in the Soviet Union during the sixties, it proved a great success in the recent years because it is easily used in industries.

This control is known by its robustness in the system. This control aims to force the system to reach a vicinity of the sliding surface and stay at this level [9]. So, we wanted to compare between these mode commands and another one to benefit from their advantage.

III.3. Witching surface

Switching function, the design of control system will be demonstrated for a following nonlinear system [8]:

$$\dot{x} = f(x, t) \times B(x, t) \times u(x, t)$$  \hspace{1cm} (8)

Where: $x \in \mathbb{R}^n$ is the state vector, $u \in \mathbb{R}^m$ is the control vector, $B(x, t) \in \mathbb{R}^{m \times m}$.

It's possible to define a set $S$ of the state trajectories $x$ such as:

$$S = \{(x(t))|s(x, t) = 0\}$$  \hspace{1cm} (9)

The following two conditions have to be satisfied:

$$s(x, t) = 0, \dot{s}(x, t) = 0$$

The control law satisfies the precedent conditions is presented in the following form:

$$\begin{align*}
U &= U_0 + U_{eq} \\
U_{eq} &= K \times \text{sign}(s(x, t))
\end{align*}$$  \hspace{1cm} (10)

Where $U$ is the control vector, $U_{eq}$ is the equivalent control vector, is the switching part of the control (the correction factor), $k$ is the controller gain. $U_{eq}$ can be obtained by considering the condition for the sliding regimen, $s(x, t) = 0$. The equivalent control keeps the state variable on sliding surfaces, once they reach it:

$$u_{eq}(x) = \begin{cases} 1 & \text{if } \quad s(x) > 0 \\
-2 & \text{if } \quad s(x) < 0 \\
0 & \text{if } \quad s(x) = 0 \end{cases}$$

$$s(x_0) = \begin{cases} \frac{x_0}{a-1} & \text{if } \quad x_0 > 0 \\
-2 & \text{if } \quad x_0 < 0 \\
0 & \text{if } \quad x_0 = 0 \end{cases}$$

The sliding surface proposed by J.J. Slotine is used in this work:

$$S(x) = (\frac{\dot{x}}{\alpha} + \beta)^{n-1} \times \epsilon$$  \hspace{1cm} (12)

$\alpha$ : is a positive coefficient,
$\epsilon = x_d - x$ is the error.
$\alpha_d$ is the desired state.
$n$ is the system order.

III.4. Direct power control (DPC) with SMC of a BDFIG

In this section, the sliding surfaces are designed based on the active and the reactive power references given in the Eq. (5). The objective of this design is to independently control the active and reactive powers converts.

A-Choice of the sliding surfaces control

The expressions of the stator voltages according to the stator currents:

$$I_s = \frac{L}{L_s} [L_s I_s^2 - R_{eq} I_s^2 - L_{mg} \omega_b \frac{d\omega_b}{dt} - \omega_b (L_{mg} I_s^2 + L_{mg} I_f^2)]$$

$$I_f = \frac{L}{L_f} [L_f I_f^2 - R_{eq} I_f^2 - L_{mg} \omega_b \frac{d\omega_b}{dt} - \omega_b (L_{mg} I_f^2 + L_{mg} I_s^2)]$$

The surface of the control $I_{ac}$, current is defined by:

$$S(I_{ac}) = I_{ac ref} - I_{ac}$$

B-Conditions of convergence of this control

To guarantee the convergence of selected variables towards the references, the two slip surfaces need to be null as following:

$$S(I_{ac ref}) = 0, S(I_{ac}) = 0$$

Figure 6. Sliding mode control Block

Where $U$ is the control vector, $U_{eq}$ is the equivalent control vector, is the switching part of the control (the correction factor), $k$ is the controller gain.
The condition of a sliding mode control base on Lyapunov attractively (\(V_0(x) < 0\)) and the surface current time invariance (\(i_s(t) = 0\))

For \(n = 1\), the surface of the current control can be set from the equation as follow

\[
\begin{align*}
S(I^{q}_{sc}) &= I^{q}_{sc-ref} - I^{q}_{sc} \\
S(I^{d}_{sc}) &= I^{d}_{sc-ref} - I^{d}_{sc} \\
S(V_{sc}^{q}) &= V_{sc}^{q-ref} - V_{sc}^{q} \\
S(V_{sc}^{d}) &= V_{sc}^{d-ref} - V_{sc}^{d} \\
\end{align*}
\]

(16)

C- The control voltage and sign function law satisfy is presented in the following form

\[
\begin{align*}
V_{sc}^{q} &= V_{sc}^{q-ref} + V_{sc}^{q-err} + V_{sc}^{q-set} \\
V_{sc}^{d} &= V_{sc}^{d-ref} + V_{sc}^{d-err} + V_{sc}^{d-set} \\
V_{sc}^{q-ref} &= K_{q} \times \text{sign}(u(x,v)) \\
V_{sc}^{d-ref} &= K_{d} \times \text{sign}(u(x,v)) \\
\end{align*}
\]

(17)

With:

- \(V_{sc}^{q}, V_{sc}^{d}\) are the control vectors relation.
- \(V_{sc}^{q-ref}, V_{sc}^{d-ref}\) are the equivalent control vectors relation.
- \(V_{sc}^{q-set}, V_{sc}^{d-set}\) are the switching control.
- \(K_{q}, K_{d}\) are positive constant.

Finely the equivalent control voltage control is given by:

\[
\begin{align*}
V_{sc}^{q} &= \frac{1}{2}(R_{sc} V_{sc}^{q} + L_{sc} \frac{d}{dt} V_{sc}^{q} + \alpha_{q}(R_{sc} \frac{d}{dt} I_{sc}^{q} + \frac{d}{dt} V_{sc}^{q}) + \delta_{q}(L_{sc} \frac{d}{dt} I_{sc}^{q} + I_{sc}^{q})) \\
V_{sc}^{d} &= \frac{1}{2}(R_{sc} V_{sc}^{d} + L_{sc} \frac{d}{dt} V_{sc}^{d} + \alpha_{d}(R_{sc} \frac{d}{dt} I_{sc}^{d} + \frac{d}{dt} V_{sc}^{d}) + \delta_{d}(L_{sc} \frac{d}{dt} I_{sc}^{d} + I_{sc}^{d})) \\
\end{align*}
\]

(18)

The BDFIG global sliding-mode control are presented in Figure 7

![Figure 7: Block diagram of BDFIG Sliding Mode Control scheme](image)

IV. Simulation Results

Table 2 shows the electrical parameters of BDFIG

| Parameter       | Value          |
|-----------------|----------------|
| Rated voltage   | \(V_p = 220V\) |
| Pole pairs number | \(p_e = 1\)   |
| Resistance(Ω)  | \(R_s = 1.079\) |
| Self-inductance(mH) | \(L_p = 714.8\) |
| Mutual inductance(mH) | \(L_{12} = 69.8\) |
| Nominal power   | \(P_s = 2.5kW\) |
| Synchronous speed | 78.3 rad/s |

V. System results and discussions

The results obtained are a comparison between two controls Fuzzy and sliding mode control, respectively organized according to the following figures.

The Active power curve in Figure 8 illustrates that The Fuzzy control which ensures high optimization of the extracted power and greatly reduces the fluctuation around optimal value, it can be also clearly seen that Fuzzy controller demonstrates more performance than sliding mode control.

![Figure 8: Active a power response of Stator (PW)](image)

In the Figure 9, the Reactive power is set to (0VAR), it had been observed that the two controllers have similar results, but the problem of chattering is evident in sliding mode controller curve and proves that Fuzzy control is more robust and provides better performance. It can be
observed that the stator voltage and current are in opposite phases Figure 10, which shows that the machine is operating in a generation mode (\(\cos\phi = -1\)). After seeing the good tracking of the proposed set-points illustrated in Figure 9, the robustness of the structure of control against the incertitude of parameters should be checked.

![Figure 9. Reactive a power response of Stator (PW)](image)

![Figure 10. Stator (PW) voltage and current](image)

Figure 11 illustrates the change of the variable speed in step form as follows when the speed is changed between 78 at the super-synchronized speed 86 rad /s to be reduced to76 rad / s.

We observed in the Figure 6 the active power is varied between – 1200 W, – 1800 W and 1800 W it remains respectively stable at 1.5 s and 3s while the reactive power is fixed at 0 Var, from where the good tracking of the proposed control can be noted more clearly in the Figure 8 in comparison to the Figure 9.

VI. Conclusion

In this paper, we described two controls of the wind energy system equipped with Brushless Doubly Fed Induction Generator. At first, we proposed a mathematical model of the machine and generator in the form of the diagram. Then, we presented two strategies based on fuzzy and sliding mode control.

The machine obtained a good performance with the Fuzzy logic control even in the appearance of variations on target, and has high-power output efficiency. Finally, the fuzzy control has approved its robustness against speed variations in comparison with the sliding mode control that gives undesirable results.

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