INTRODUCTION

In general, the key issues regarding powders are storage and flowability problems; further areas are pharmaceutical and food mixtures preparation, various materials composites formulation as well as particle design and energy storage enhancement. In this review these issues are addressed only in those aspects which are of technological significance. The authors’ findings concerning these issues are discussed and referred to other published works within these fields.

Flow and storage problems are among the oldest questions concerning powder technology and irrespective of abundance of related literature, many of them have not yet been fully resolved. Powder flowability can be critically affected by the presence of moisture, usually in the form of small amount of water existing between powder particles. The presence of water in some cases may be the result of manufacturing conditions, or more insidiously, it could be attributed to water vapor condensation from surrounding atmosphere. The latter case is rather unexpected and usually unpredictable and it may lead to substantial changes in the processing characteristics of powders and, in some extreme cases may be a reason to stop the process control [1, 2].

In the first part of the review, the rheology of moist powders of different nature (chemical, pharmaceutical, food, solid biomass and biomass-coal mixtures) as processed in static and dynamic conditions is discussed. The studies undertaken in static conditions are usually referred to storage of...
powder in silos and the crucial question is how the process of silos discharging should be arranged. Dynamic conditions, on the other hand, are referred to processing of particulate solids in flow operations in various process industries where the fundamental issue is ability of powder to flow in a controlled and predictable manner. The variety of materials under investigation, wide range of their dimensions, physical and chemical properties and water content in experiments performed allowed the main factors influencing the powder rheology to be identified regarding specific group of powders, tests conditions, properties of solids, water content, powder blends proportion and others.

In the second part of the paper some new areas of powder exploration and the resulting challenges are presented. These include mechanochemical approach to powder particles physical modification and/or reactive alteration. Improved parameters of bulk operations and preparation of composite materials of strengthened physical or chemical properties are some of examples. The mechanical energy transitions of solids have a notable advantage since technologies realized mechanochemically do not require organic solvents and elevated pressure and temperature. Among the areas where mechanochemistry finds its successful practical implementation is also cohesive powder flowability improvement which is further discussed.

A relatively new mechanochemical approach to powder flow improvement is high-energy ordered mixing (HEM) (or interactive mixing) consisting in doping the agglomerated powder bed with small amount of finely comminuted, typically nano-sized additive and delivering to the bed some mechanical energy. This is typically accomplished using planetary ball mill/mixer (PBM) and the mixing in such environments is a multi-parametric process that demands optimization of the process parameters values. For that purpose design of experiment (DOE) technique and response surface methodology (RSM) were used. Following-up the optimization procedure the mixing parameters values can be found at which the powder flowability is significantly increased. This findings may be a basis for developing a general routine allowing the optimal parameter values of high-energy mixing in planetary ball mill to be credibly predicted regarding some physical properties of powders only with a limited number or no experiments needed. The successful use of such approach was demonstrated in experiments carried out for Naproxen doped with nano-sized Aerosil additive.

In the third part of the paper powder flow modelling is discussed mainly in the context of the relevance of DEM method for powder flow prediction and common problems encountered using this method as well. The most often reported problems are high computational cost required for systems of large number of particles interacting in a powder bed and strong dependence of DEM response on employed contact model and particle properties as the inputs. The proposed solutions are generally of limited effectiveness and in authors’ opinion the DEM is a valuable tool to examine particulate systems but still on a microscope scale, i.e. limited to the particle-particle or particle-wall interaction analysis instead of using it to powder mass flow predicting. Rather than try to transform the calculated microscopic parameters of individual particles, like velocities and positions into more or less reliable macroscopic behavior of the whole bed, it certainly seems possible to use the features of DEM method to verify some uncertain input data, e.g. particle properties values. This often applies when modelling the rheology of moist powders consisting of particles of hygroscopic properties, like in the case of many plant materials. The moisture can substantially change the properties of powder bed particles and this is often not accommodated during routine DEM calculations, except for a few examples [3, 4]. As a result the calculated data deviate substantially from those obtained experimentally and the level of the observed discrepancy could be a reliable measure of the rheological characteristics alteration due to moisture content in a powder bed.

POWDER FLOW PROBLEMS

Many attempts to study the rheological behavior of a cohesive powder have been undertaken and no general approach to flow improvement is given so far. A possible reason is a large number of factors influencing powder behavior. These include variety of existing methods to study ability to flow, different types of powders and their properties, as well as changeable surrounding conditions and different processing and storage parameters. An example of the diverse attitude to powder research may be a recent review on various methods of flowability
evaluation, as given by Ogata [5]. Hence, in this Chapter the factors influencing powder flow will be discussed separately in various categories of materials of different properties and economic use, like industrial goods, agricultural products and biomass energy-based resources.

Rheology of moist powders

The use of powders, irrespective of their nature, is commonly accompanied by moisture, usually water transferred from surrounding atmosphere to powder bed [1, 2]. The increase of water amount on particle surfaces gradually increases the particle contact area and causes the powder to become more cohesive. This, however is the case only for powders being in static conditions like those stored in silos.

Powder materials bed in motion may be in various rheological states. If the bed is subjected to low shear rates, its behavior cannot be described by the behavior of either liquid or solid. Such a state is referred to as the friction state or the Coulomb state [6]. In this state, the stress in material is created by friction of the particles in contact with each other. For high shear rates, individual particles have a sufficiently large energy reserve to allow the bed to behave in a way similar to a free-flowing liquid [7]. Static methods of testing powders provide information about their behavior under considerable external load and a negligible low deformation rate. Dynamic methods of testing powders provide information on their behavior under low external loads and high deformation rate.

In dynamic conditions, when powder is flowing under some external forces the increasing moisture content affects the flowability in the opposite way. These questions will be examined for all the three mentioned groups of powders and some new methods of flow improvements will be given.

Rheology in static conditions

An indication of potential powder flow properties in static (quasi static condition) is powder yield strength which was measured with Jenike-type shear-tester fabricated and used in accordance with the CEN Eurocode 1, 2006 procedure [8]. The schematic of the apparatus is shown in Fig. 1. The dimensions, operating principle and experimental protocol of the experiments

![Fig. 1. Schematic representation of the Jenike-type shear tester. 1 – drive engine, 2 – drive pin; 3 – lever bar; 4 – lever; 5 – normal load; 6 – shear stress transducer; 7 – base; 8 – movable shear cell; 9 – arm of immovable shear cell; 10 – immovable shear cell; 11 – twisting cover](image)

![Fig. 2. The effect of moisture content on yield loci for limestone (36-100 μm), σn = 80.3 kPa](image)
performed with this equipment are given in earlier paper of the authors [9, 10].

With increasing moisture content, growing shear stresses in the bed were developed and mechanical strength of the moist bed was built involving resistance to flow to be larger. Measurements of shear strength were carried out using a consolidating stress value such that the material is sufficiently compacted. Some typical examples of this effect for selected materials from all these groups are shown in Figs. 2 to 5.

Similar results [11, 12] were obtained for other tested materials, like microcrystalline cellulose (Avicel 50 - 150 μm), silica gel (40 - 63 μm), PVC (150 - 250 μm), glass beads (250 - 500 μm), modified limestone (36 - 100 μm), amaranth (750 - 2000 μm), mustard (1000 - 3000 μm), millet grains (1000 - 2500 μm), wheat flour (36 - 150 μm), corn starch (50 - 200 μm), potato flour (36 - 750 μm), milk powder (75 - 250 μm), pine- (10 - 550 μm), oak- (170 - 720 μm), and cherry- (85 - 580 μm) sawdusts, sawdust mix (60 - 530 μm), MDF sawdust (45 - 725 μm), sunflower shells (180 - 800 μm), apple pomace (250 - 2000 μm), DDGS (Distillers Dried Grains with Solubles, 5 - 600 μm), meat and bone meal (150 - 2000 μm), hard coal (3 - 85 μm) and brown coal (10 - 115 μm). In all mentioned figures the moisture content $s$ is defined as the ratio of water mass $m_w$ and dry powder mass $m_p$ as follows:

$$s = \frac{m_w}{m_p} \cdot 100\%$$

Rheology in dynamic conditions

Rheological characteristics of powders in dynamic conditions can be tested using a powder rheometer. There are few types of this relatively new equipment featuring of some innovative qualities. One of them is FT4 powder rheometer [13÷16]. It was applied to evaluate the powder flowability based on the total energy input which is related to the shear stress developed on the rheometer impeller blade. This construction is widely used to determine flow properties of industrial powders [17, 18], pharmaceutical solid dosage forms [19, 20] and also lignite [21]. New approach to determine powder flow is Anton Paar two cells powder rheometer with powder shear cell and powder flow cell [22]. The powder shear cell with temperature and humidity control is used to determine the flow characteristics of consolidated powders and their time-dependent behavior. The powder flow cell is an innovative
approach towards powder characterization in dynamic condition. The dynamic properties of powders can be also examined with a rotating drum tester – Granudrum powder rheometer [23]. This construction is used to study the dynamic flow properties of powders such as dynamic angle of repose and dynamic cohesivity index. The flowability of powder measured as a function of the shearing rates of the cell (rotating speed) allows for evaluating rheological properties such as shear thinning or shear thickening.

In this work an annular shear cell-type powder rheometer was used [24] and a simplified draft of this apparatus is given in Fig. 6. The design of the rheometer was based on that proposed earlier by Klausner et al. [25]. The construction details and operating principle were given elsewhere [24, 26] and here only the most important features of the apparatus are given.

A unique quality of this rheometer is that the level of shearing is confined to the thickness of shearing band of powder bed alone, and this is usually not more than 15-20 particle diameters [25]. Thus, the real conditions of powder bed shearing are met, i.e. the shear stresses are measured for the particles moving in a shear band, rather than over the whole bed. Hence the data obtained in experiments can be reliably compared with those calculated theoretically.

The shear stresses measured with the rheometer, i.e. under low normal loads, changed with moisture content in an opposite way as compared to those measured with Jenike tester under high loads in static conditions [12]. With increased moisture content, the flow properties of majority of the tested powders and granular materials were clearly and regularly getting better as seen in Figs. 7 to 10.

![Fig. 6. Sketch of the annular powder rheometer: 1– shear plate positioner, 2 – normal load transducer, 3 – shear plate, 4 – tangential load transducer, 5 – annular gap, 6 – displacement transducer, 7 – rotating cell, 8 – driving gear](image)

![Fig. 7. The influence of moisture content and shear rate $\dot{\gamma}$ on shear stress $\tau$ for PVC powder (75 - 150 µm)](image)

![Fig. 8. The influence of moisture content and shear rate $\dot{\gamma}$ on shear stress $\tau$ for semolina (100 - 250 µm)](image)
Regardless of regularity in powder rheological characteristics as shown above, there were also some exemptions in terms of moisture content affecting powder rheology. This usually concerned fine powders and/or particles of hygroscopic nature. An example is limestone powder (particle diameter 36-100 µm). Rheological characteristics of the limestone without any surface modification is shown in Fig. 11, and after modification with a SARSIL (silicone impregnate to prevent water absorption) as surfactant – in Fig. 12.

Unexpectedly, the moisture affected the rheology of unmodified limestone powder unfavorably, i.e. in the opposite way as it was for other industrial materials. Under the surfactant influence, the behavior of modified limestone powder was turned towards a typical rheological pattern.

A possible explanation of this effect may be given on the basis of specific surface properties of the limestone used and some experimental data on this may be found in paper by Vogt and Opaliński [27]. In more general terms it may be referred to the observed diversity in rheological characteristics obtained under high or low normal load, i.e. static or dynamic conditions. In static conditions (with Jenike’s shear tester) the powder bed is under high external normal load and the stresses developed in the bed are overwhelming and suppressing any other particle interactions (thus no difference in rheology of unmodified and modified limestone was observed). When the bed...
is in dynamic conditions (examined with powder rheometer), the stresses developed from low normal loads are small. As a result, some weaker interparticle interactions can be exposed, as seen in the case of surface modification of limestone particles (a lubricating effect is possible to appear due to presence of surfactant).

Similar rheological exception concerning moist powders sheared in dynamic conditions (using powder rheometer) has been observed in the case of potato starch – Fig. 13. As opposed to other materials, both of these used in process industries and in agriculture, the effect of water content proved to be obviously unfavorable. Other examples of such rheological exemptions (tough not always as obvious) are milk powder and wheat flour [24].

It is believed that this reverse moisture impact on powder rheology may be a result of hygroscopic nature of materials. The fine, hygroscopic particles of potato starch or milk powder absorbed moisture into their grain cells thus preventing the water film between particles to be formed and lubrication effect to be developed as it was found for majority of the materials investigated (see Figs. 7 to 10 and 12). Another effect of water absorption by biomass particles may be that moist biomass particles become soft and swollen. As a result, particle contact resistance increases and the powder flow is transformed from the stream of freely moving particles to slow, frictional flow of powder bed of larger mechanical strength.

A separate part of the performed research was related to biomass solids due to growing interest in the sustainable and increased use of renewable energy sources. One of the primary troubles found when using powdered solid biomass is a negative impact of moisture content on physical properties of biomass grains [28]. The other concern is unsatisfactory flowability of biomass as compared to conventional solid fuels (e.g., granular or fine coal). A possible way to improve the bio-fuel flowability is to use the comminuted biomass in a mixture with coal [29].

As it is emphasized in the literature [30], the satisfactory flowability of the mixture is the key factor determining the efficiency of co-combustion processes.

On the basis of performed experiments using Jenike shear tester (static conditions) or powder rheometer (dynamic ones) it was found that rheological characteristics of moist biomass samples was equally advantageous as it was for industrial powders and that the moisture impact was particularly effective when moisture content exceeded rather high values - above 20% [31].

It was also found that rheology of biomass sample mixed with hard coal was better than it was for the components examined separately. This effect can be explained on the example of sawdust as solid biomass blended with hard coal as a conventional fuel. The main component of the solid biomass used was pine sawdust (60%). Remaining components were beech-, oak- and sycamore sawdust. This biomass composition will be further referred to as industrial sawdust mixture. The effect of water content on shear stress for hard coal is shown in Fig. 5 and for industrial sawdust

![Fig. 13. The influence of moisture content and shear rate $\dot{\gamma}$ on shear stress $\tau$ for potato starch (36 - 750 μm)](image)

![Fig. 14. The effect of moisture content on yield loci for industrial sawdust mixture: pine sawdust 60%, beech sawdust 20%, oak sawdust 10%, sycamore sawdust 10% (60 - 530 μm) $\sigma_n = 22.2$ kPa)](image)
characteristics of coal - Fig. 15. Increasing the content of biomass in the mixture reduces the adverse effect of moisture on the strength of the mixture and improves its flowability - Fig. 16. Similar results [12] were obtained for other tested mixtures, like DDGS and meat and bone meal mixtures with hard coal.

This positive impact of biomass with coal mixing may be related to water absorption by biomass particles. As the water amount in the mixture is lessening, the unfavorable effect of moisture content on rheology of moist hard coal is weakened (see Fig. 5), so the mixture flow is better. This leads to an interesting conclusion about the stabilizing effect of biomass on the mechanical properties of its mixtures with coal.

If the admixture of sawdust to coal is small, e.g. 5%, the mixture characteristics are unfavorable and deviate to a small extent from the flow characteristics of coal - Fig. 15. By comparing the data given in the Fig. 5 and in Fig. 14 it is clearly visible that dry coal has a good flowability, while wet coal flows badly, much worse than biomass, not only dry, but also moist. The high concentration of the yield loci lines for the sawdust mixture shown in Fig. 14 means that the moisture content has less influence on the mechanical strength of the biomass bed and this biomass property can be used to improve its flowability and, in the end-use, its co-combustion conditions with coal.

![Fig. 15. The effect of moisture content on yield loci for mixture of sawdust (5 mass. %) and hard coal (95 mass. %)](image15)

![Fig. 16. The effect of moisture content on yield loci for mixture of sawdust (60 mass. %) and hard coal (40 mass. %)](image16)

![Fig. 17. Shear stress-displacement relationship for potato starch; water content $s = 5\%$, $\sigma_n = 23$ kPa](image17)

![Fig. 18. Shear stress-displacement relationship for potato starch; water content $s = 15\%$, $\sigma_n = 23$ kPa](image18)
Therefore, the operations accompanying the process of biomass and coal co-firing can be carried out more safely and within wider range of humidity (difficult to control) values. This may be of significant importance for biomass logistics and also for handling and other operations concerning the mixtures being delivered to boilers or burners.

**Flow singularities**

In the context of the discussed regularities regarding the effect of moisture content on powder rheological characteristics, there are some interesting flow singularities. One of them involves shear stress oscillations clearly revealing in dry powder during shearing. The oscillation weaken when the powder is moistened and finally disappear at higher moisture content. This is shown in Figs. 17 and 18 for potato starch [7, 11].

The oscillations seen in Fig. 17 mean that across a small distance of the powder bed there are large variations in the shear strength. The oscillations may result in silo walls vibrations (“silo music”) as well as in a local increase of the bed density and its strength. Both of these factors are risky for storage equipment construction and hazardous for operating staff and environment. Some reasons for oscillation development in sheared powder bed are given elsewhere [7].

Other powder rheological oddness identified when powder was sheared in static conditions, is appearance of “lubricating point”, i.e. the moisture content value at which the influence of moisture content on rheological characteristics of powder bed becomes reversed [7, 10÷12]. This took place usually at higher moisture content (above 10%) and it was observed for some materials of all the three groups, e.g. glass beads, rapeseed, DDGS with brown coal mixture and others. Particularly clearly it was noticed for rapeseed and it is pictured in Fig. 19 [10].

An acceptable explanation of the lower values of shear stresses observed in the bed of rapeseed of larger water content is as follows: when moisture content becomes higher, some amount of free water appears in the bed as it cannot be absorbed by smooth and hard rapeseed surface any longer. The water layers lasting on the bed particles can in an obvious way result in particle surfaces lubrication and powder bed strength reduction.

Another interesting rheological feature related to some moistened powder samples tested in dynamic condition was “sharp flowability increase” caused by increasing moisture content at low values of shear rates. The essence of the event is presented in Fig. 20 and it is typical outcome for many studied mixtures of biomass with coal [12].

This may be related to a complex effect of frictional flow mechanism coupled with lubrication effect in slowly moving dense powder bed. From technological point of view this factor is of significant importance as it allows processes with powders to be economically realized.

**IMPROVEMENT OF POWDER FLOWABILITY**

Flowability, as a property of fine powders especially important in powder handling and processing,
is still investigated and improved. Many methods for powder flow improvement were used so far. Good examples are different methods of granulation applied in food, pharmaceutical or chemical industries [32–35]. Other methods toward enhancing powders flowability were mixing the powders with additives of various nature [36–40]. The mixing methods are particularly effective when using them in the form of mechanochemical technique of high-energy ordered mixing (or interactive mixing). The additives needed in the mixing process are most often inorganic oxides (e.g. fumed silica) and they are assigned to reduce the adhesive interactions between particles in the powder bed. Some salts of fatty acids (e.g., magnesium stearate) can be also applied as lubricants, being adsorbed on the surface of powder particles in the form of a monolayer. Due to additives cohesiveness and their tendency to agglomeration there is a problem to disperse them uniformly in the mixture during conventional blending. Hence high-energy mixing, called also dry coating or mechanofusion, has been employed as a more effective, environmentally and simpler method of improvement of powder ability to flow [41]. This relatively new mechanochemical approach consists in doping the agglomerated powder bed with small amount of finely comminuted, typically nano-sized additive and delivering to the bed some mechanical energy. If the amount of energy is large enough, the agglomerates of both the bed and admixture particles are breaking apart. In the next stage the bed (host) particles are covered by admixture (guest) particles that makes van der Waals forces much weaker from those original ones previously existing in the agglomerated bed and flow properties of the resulting mixture improve [42, 43]. The effect of dry coating process is schematically presented in Fig. 21 and an example of surface changes after dry coating (obtained by the authors) is given in Fig. 22 (SEM images).

To perform the dry coating process, it is necessary to use some devices which are able to generate a great amount of mechanical energy, which is sufficient to break up the agglomerates of host and guest particles and to enable numerous collisions between them to exist. There are many methods and devices to perform high-energy interactive mixing and those especially advanced are manufactured in Japan, e.g. Mechanofusion by Hosokawa Micron, Hybrydizer by Nara Machinery or Theta Composer by Tokuju Company. Background of dry coating as well as different methods and devices have been previously widely described in the literature, e.g. by [44, 45] and the reader is referred to this literature.

High-energy interactive mixing as a method of powder flowability improvement is mainly used for pharmaceutical powders. Over the last decade Zhou and co-workers extensively investigated the influence of dry particle coating on flowability of many pharmaceutical powders. One of the first works of this research team concerning mechanofusion was focused on the improvement of flowability of lactose monohydrate powder doped with small amount of fumed silica or magnesium stearate. For that purpose Nobilta mechanofusion system (Hosokawa Micron) and tumbling mixer [46] were applied. The results confirmed that mechanical dry particle coating is more efficient than traditional tumbling blending. In the subsequent works Zhou et al. proved that host particle size larger than 20 µm [47] and process conditions, providing greater amount of energy to the powder bed [48] have significant influence on surface modification and powder flow improvement. Moreover, it was found that the higher content of MgSt (up to a level of 5% w/w) on the bed particle surfaces, the stronger reduction of cohesive forces [49].

![Fig. 21. Schematic representation of dry coating process](image-url)
The literature data indicate that the mechano-fusion also seems to be an effective method of improving aerosolization of API (e.g. salbutamol sulphate, salmeterol xinafoate, triamcinolone acetonide) and inactive additives (lactose) in dry powder inhalers systems as a result of cohesive-ness reduction [50÷52].

The effect of different guest particles (MgSt, silica, L-leucine, sodium stearate fumarate) on dissolution and flowability of fine ibuprofen powder has been examined by [53]. They demonstrated successful flowability enhancement in case of all investigated admixtures and showed that it depends mainly on surface coating effects instead of particle shape or size modification.

Active pharmaceutical powders were also dry coated using magnetic forces. Three API’s with different shape and size: ibuprofen, acetaminophen and ascorbic acid were processed in magnetically assisted impaction coater (MAIC). Hydrophilic or hydrophobic nano-silica as invited particles were used in the work by Jallo et al. [54] and the authors managed to successfully transform even very cohesive powders to that of easy flowing.

To perform the dry coating process, some conventional pharmaceutical high-shear mixers or mills were also employed. Sato et al. [55] investigated how operation conditions in Cyclo-mix affect pharmaceutical excipients properties like Suglets during coating by MgSt. Regarding the flowability they showed that filling ratio was not important factor but longer processing time and higher rotating speed had significant influence on powder ability to flow. Mullarney et al. [56] successfully applied another high-shear mixer: conical screen mill (Comil), to perform high-energy mixing in laboratory and pilot scale. They obtain dry coating effect as well as flowability enhancement by mixing excipients (mannitol, lactose monohydrate) and active ingredients like ibuprofen and another five APIs with silica. Huang et al. [57] confirmed application of Comil as a continuous-action device to improve pharmaceutical powders handling and processing. Han et al., [58, 59] obtained successful results in improving properties (e.g. flowability) of pharmaceutical blends using API (ibuprofen) after dry coating in Comil or dry coating and simultaneous micronization in fluid energy mill.

Pharmaceutical industry is not the only branch where problem of powder ability to flow is of such importance, but high energy-mixing in other branches is not as popular as it is in drug preparation. However, there are few works concerning powder flow enhancement via dry coating. For example, Ramlakhan et al. [60] applied dry coating in MAIC to improve handling of cornstarch powder and cellulose fibers using nano-silica as guest particles. Similarly they used nano-alumina powder as an additive to dry coat PMMA particles. Cohesive corn starch was also processed by Yang et al. [61] using MAIC and hybridizer. MAIC also turned out to be effective device to decrease cohesion between host aluminum particles via high-energy mixing with nanoparticles like silica, carbon black and titania [62]. Dry coating seems to be effective method of preparing polymers fillers, and calcium carbonate is an example. Simultaneously coating by silica and milling in fluid energy mill conducted by Qian et al. [63] reduced cohesion and increased flowability of CaCO₃.
A promising device to perform high-energy mixing with the aim to ensure cohesive powders flowability improvement via dry coating is a planetary ball mill. For the first time it was proposed as a device to perform dry coating of powders by Sonoda et al. [64] to improve solubility of flurbiprofen powder in water. This type of mill consist of one or several grinding chambers attached to a rotating disc and filled with grinding balls. The large amount of mechanical energy which is needed to obtain dry coating effect is generated as a result of planet-like movement of the working chamber. This type of movement enforces the balls to move inside the chamber as well as provides the balls with large acceleration and frequent collisions.

The use of planetary ball mill for grinding or carrying out mechanochemical processes has been known for many years. However, until the 1990s, it was limited to laboratory purposes only. Furthermore, it was assumed that it is not possible to scale up the process. The problem of increasing the processed volumes of powders, as well as the continuous action of the planetary ball mill has been successfully solved over the past decades. Currently, this type of mill with a productivity of up to 5 t/h and continuous action are designed and manufactured mainly in Russia [65].

In the works by the authors a planetary ball mill was used for flowability improvement of cohesive powders, used mainly in chemical, pharmaceutical and food process industries: calcium carbonate [66], Apyral [67], Disulfiram (Esperal) [68] and potato starch [69] powders. The powders were doped with nano-sized silica (Aerosil) and also with propan-2-ol as a process control agent (PCA), needed to avoid caking of fine powders during their mixing. To provide the right conditions for powder processing, an optimization of process parameters was accomplished. The optimal mixing parameters were specified using statistical procedures: response surface methodology and central composite rotatable design. Mathematical model equations describing the influence of input variables (mixing speed and time and the amount of additives used) on powder flowability indices (output variables) were based on the second order polynomial equation (Eq. 2) for coded levels of variables.

\[
y = (b_0 + \varepsilon) + \sum_{i=1}^{k} b_i x_i +
\]

\[
+ \sum_{s=1}^{k} b_{ij} x_i x_j + \sum_{i=1}^{k} b_{ii} x_i^2
\]

In the model above \( y \) is a flowability index (angle of repose or compressibility index), \( b_0 \) – constant term, \( \varepsilon \) – residual associated with the experiments, \( x \) – process variable and \( k \) – number of process factors. The results were presented on 3D response surface plots (converted to actual levels of variables) as it is shown in Figure 23.

The response surface methodology as illustrated above was successfully applied for all the aforementioned powders, however the full statistical procedure and results obtained for Disulfiram are not given here since they are intended for separate publication in the near future.

Model optimization of multi-parametric process, as is the case with interactive mixing, is difficult to formulate due to several local minima [66, 67, 69]. For that reason, to perform the process optimization, the authors’ suggestion is to convert the model equations to a desirability function. The specific feature of the function is that its maximum can be attributed to the best powder

![Figure 23](image-url)
flowability, i.e. the smallest values of flowability indices (angle of repose and compressibility index). Following-up the optimization procedure the mixing parameters values and the amounts of applied additives are found at which the powder flowability was significantly better as it was originally. This findings may be a basis for developing a general routine allowing the optimal parameter values of high-energy mixing in planetary ball mill to be successfully predicted regarding some physical properties of powders only with a limited number or no experiments needed. The accuracy and reliability of the proposed procedure were successfully verified in experiments carried out for Naproxen doped with nano-sized Aerosil additive (to be published).

POWDER FLOW MODELLING

In the recent years the Discrete Element Method (DEM), resumed by Cundall and Strack [70], has become the most attractive and preeminent numerical technique to perform modelling of powder flow and designing of powder handling processes by taking advantage of significant computer hardware and computing capability development. Following the Lagrangian principles, the DEM allows tracking of each entity within a powder bed and predict macroscopic powder flow behavior as a result of microscopic activity of the individual particles in an assembly. Alternatively, continuum based methods such as the finite element method (FEM) are also applied but may fail to model such artefacts as large deformations or segregation associated with granular materials [71]. The DEM algorithm makes use of Newton’s second law of translational and rotational motion to determine powder bed changes basing on the forces acting on each particle (or granular media entity) in the contact points between them. The contact model describing particle-particle and particle-geometry interaction determines the modelling process, hence its selection is crucial in the correct real systems representation. According to the contact models available in literature, the contact forces are functions of particles’ overlap distance and other micro level parameters: particle size and shape, particle density, particle contact stiffness, contact damping and friction coefficients. Further model improvements may involve additional attractive and repulsive interactions (i.e. those caused by interstitial liquid or electrostatic charges). This method is effective in modelling of dense systems and referred to as the soft-sphere approach in contrast to the hard-sphere approach more applicable in sparse dynamic systems [72, 73].

Since there is no generalized theory on granular materials which reliably predicts their behavior, numerical simulations can be used to predict and to optimize the processes in powder technology prior to industrial implementation. Fundamental advantage of the DEM is that it provides insight into the mechanisms governing particles flow in a variety of powder handling processes and is a powerful tool that enables recording of any required parameter also those difficult or impossible to measure in laboratory conditions. As a result DEM facilitates understanding granular dynamics and development of generalized rheological models [74, 75].

However, the computational requirement of DEM simulations for predicting real scale bulk flow resulting from contact detection and implicit integration problems is the main constraint inhibiting DEM analyses with numerous sets of particles and realistic particle geometries. Thus, despite introduction of dedicated computer hardware architecture based on multiplication of processor cores and parallelization of DEM code procedures by using subdomains or clusters [76] the DEM analyses are still limited to simplified cases (systems) or the micro level particle-particle or particle-wall interaction analysis. Another important constraint in effective DEM application is selecting appropriate input parameters so that simulations can accurately reproduce the behavior of real systems. Therefore a robust calibration procedure is indispensable prior to the simulation for real application purposes. Although the calibration process is a crucial step of every correct simulation, it is also a factor extending the time required to obtain a valuable prediction.

Direct and indirect methods are available in literature for DEM model calibration [71]. In the first approach, the particle properties are measured by experiments and then directly used as simulation input parameters. In indirect calibration, a bulk property (or performance) is registered, and then a set of simulation parameters is adjusted until the measured bulk properties match the desired real response of the studied system. Since the micro level properties are hard to measure, and frequently are not adequate when applied on a bulk level, the indirect procedures are dominant and referred to as the inverse calibration methods [71, 77].
The calibration procedure was found necessary in the recent research regarding powder shear flow modelling using DEM. For example, Simons et al. [78] recognized Young’s modulus, the static, and the rolling friction coefficients as the most influential particle parameters in the observed tangential shear stress at steady state flow in the performed sensitivity analysis using the Schulze ring shear tester. The critical role of the static and the rolling friction coefficients affecting powder shear resistance expressed as basic flowability energy (BFE) and specific energy (SE) was confirmed in [79] and [80] during DEM calibration procedure for Freeman FT4 rheometer since it has become as a widely used technique for characterizing particle flow. The impact of inter-particle static and rolling friction coefficients and the resulting requirement for proper calibration of these parameters in the DEM simulation was shown also in other experiments involving powder shear flow including e.g. silo discharge [81], oedometric compression tests [82] or uniaxial compression tests [83].

The well-known effect of moisture content on bulk powder rheology via capillary cohesion forces was described and introduced to the classical \(\mu(I)\) rheology [75], however only for materials resistant to water sorption and internal diffusion. The problem of hygroscopic materials of biological origin and alteration of their properties along with moisture was studied in [12]. At low level of water content these materials tend to absorb water and swell up to the point of saturation. Only exceeding the saturation point means starting the interstitial water adsorption process and formation of liquid bridges. For explanation of such phenomena on powder bed rheology below saturation point the swelling bed model assuming linear effect of moisture content on the bio powder properties (particle density, volume and elasticity module) has been proposed and verified with DEM [12]. The increase of compressive stress obtained by DEM in the case of DDGS with 30% moisture content compared to dry DDGS material is shown in Fig. 24.

The results obtained in [24] for semolina of particle size (0.1-0.3 mm) support the idea that friction coefficients and damping factor of particulate materials are not constant and that they are significantly reduced at higher moisture content of the powder bed in the whole range of shear rates applied due to modification of outer particle surface properties (Fig. 25). The values of the friction coefficients as well as damping factor that had to be adjusted during the DEM simulations to...
fit the experimental data can be treated as a quantitative measures of material’s rheological properties. Sharp decrease of both friction coefficients for moist material (as shown in Fig. 26 for the semolina case) could be an indication of material surface properties modification followed by powder rheology changes, under assumption that the applied DEM contact model is correct.

The obtained results are a premise to continue the experimental verification and possibly generalization of rheology models based on DEM simulations in the range of high shear rates as well as for moist powder conditions. There are several necessary conditions for further progress. First is the increase of computing power of modern computers both by parallelization of multiple computing units particularly when the Moore’s law of a doubling in processor performance every 18 months is no longer valid. In this regard application of the graphical processing units (GPUs) accelerating calculations, as shown in [84], and further optimization of DEM code may be of utmost importance. Secondly, the implementation of effective techniques for a DEM model calibration as well as for DEM code optimization. Among already confirmed procedures are Design of Simulation (DoS) techniques based on the idea of Design of Experiment (DoE) [80, 85, 86], artificial neural network (ANN) approach [77, 86], Bayesian filtering [82], or Young’s modulus reduction [87]. Thirdly, focusing on hybrid continuum constitutive modelling (such as FEM) coupled with DEM approach to fully utilize the advantages of both ideas and to avoid or mitigate their respective drawbacks that has already resulted in promising results [88÷90].

CONCLUSIONS

Rheology of moist powders is affected to the greatest extent by conditions the powders are operated. In static conditions that usually apply to powders storage, the increase in powder bed moisture definitely promotes the bed consolidation and obstructs the emptying of storage equipment. In dynamic conditions relevant to powder flow under low external forces, the moisture makes flow of many powders easier.

Exemptions from the trends specified above are likely to happen for powders composed of fine particles of hygroscopic nature and of modified surface properties and they were found in both static and dynamic conditions. In static ones these included development of shear stress oscillations in the bed with low or no water content as well as appearance of lubricating effect found for some smooth and hard (rapeseed) particle surfaces. On the other hand, in dynamic conditions it was observed that at low values of shear rates the flow increased sharply with moisture content increase and also that the rheological characteristics of moistened powders with modified surface properties was reversed.

Small amount of water content favorably affects the rheology of moist powders; damaging oscillations are markedly diminished or removed and the processes with powders handled under low external forces proceed smoothly.

Of the results obtained, those concerning biomass-coal mixtures are of practical meaning. Supplementing the moist bed of coal with solid biomass improves the mixture flowability and stabilizes its mechanical strength i.e. makes it more resistant to moisture content changes. Thus the...
operations associated with biomass and coal co-firing can be carried out more safely and within wider range of unforeseeable humidity values.

Flow improvement still remains the challenge particularly with regard to nano-sized powdered materials which are of increasing importance to many branches of industry. A continued development of particle design approach and more progress and innovation with industrial-scale high-energy mixers operating possibly in a continuous mode seem to be the most recommendable lines of action for the future.

The obtained results are a premise to continue the experimental verification and possibly generalization of the way the DEM method is used to solve powder rheology problems. Further proceeding should cover a holistic approach including both techniques for calculations acceleration and also those numerical procedures, which coupled together allow to fully utilize their advantages and to avoid or mitigate their respective drawbacks.

Nomenclature

| Symbol | Name                             | Unit     |
|--------|----------------------------------|----------|
| API    | Active pharmaceutical ingredient |          |
| ANN    | Artificial neural network        |          |
| DEM    | Discrete element method          |          |
| DoS    | Design of simulation             |          |
| DoE    | Design of experiment             |          |
| FEM    | Finite element method            |          |
| GPU    | Graphical processing units       |          |
| PMMA   | Poly(methyl methacrylate)        |          |
| SEM    | Scanning electron microscope     |          |
| $b_0$  | constant term of polynomial equation | [1]     |
| $d_p$  | particle diameter [mm]           |          |
| $I$    | inertial number [-]              |          |
| $k$    | number of process factors in Eq. 2 [-] |         |
| $p$    | pressure [Pa]                    |          |
| $s$    | moisture content in powder [mass%] |         |
| $x$    | process variable [-]             |          |
| $y$    | shear rate [1/s]                 |          |
| $\mu$  | apparent friction coefficient [-] |          |
| $\mu_s$| static friction coefficient [-]  |          |
| $\mu_{rol}$ | rolling friction coefficient [-] |          |
| $\epsilon$ | residual associated with experiments in Eq. 2 [-] | | |
| $\sigma$ | normal stress [Pa]               |          |
| $\tau$ | shear stress [Pa]                |          |
| $\phi$ | internal angle of friction of a powder bed [deg] | | |

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