The Evolution of Homophily

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Biologists have devoted much attention to assortative mating or homogamy, the tendency for sexual species to mate with similar others. In contrast, there has been little theoretical work on the broader phenomenon of homophily, the tendency for individuals to interact with similar others. Yet this behaviour is also widely observed in nature. Here, we model how natural selection can give rise to homophily when individuals engage in social interaction in a population with multiple observable phenotypes. Payoffs to interactions depend on whether or not individuals have the same or different phenotypes, and each individual has a preference that determines how likely they are to interact with others of their own phenotype (homophily) or of opposite phenotypes (heterophily). The results show that homophily tends to evolve under a wide variety of conditions, helping to explain its ubiquity in nature.

Homophily, the tendency to interact with others of similar type, is widely observed in nature. Sex- and age-related homophily, for example, shapes the formation of clusters of preferred companionships in zebras1, dolphins2, and predicts both the quantity and quality of many primate interactions3,4. Meerkats tend to assortatively associate with other group members of similar attributes in dominance and foraging networks5. And across many dimensions of phenotypes, humans exhibit high levels of homophily in social tie formation6–8. In fact, recent evidence suggests that humans may even exhibit genotypic homophily, meaning that individuals with a certain genotype are more likely to be friends with others of the same genotype9.

Heterophily, the tendency to interact with others of different type, also exists in nature at both the cellular10–12 and organismal levels. For example, research on collaboration networks suggests that people are likely to form heterophilic task-related ties with those who are complementary to their own skill sets13. Analogously, hunter-gatherer life is characterised by long-term imbalances in productivity and consumption, and by the division of labour14; hence, one might possibly expect that social interactions would, at least in part, be heterophilic, offering complementary advantages to interacting parties; but they are not15.

Indeed, heterophily is far less common than homophily. Much effort has focused on examining the functional role homophily plays in a wide range of domains, including social segregation16, cultural polarization17, friendship formation18, social contagion19, and the evolution of cooperation20,21. And the ubiquity of homophily suggests that natural selection may favour it. Yet, to our knowledge, there have to date been no attempts to understand the possibly evolutionary origin of this phenomenon.

Here, we conceptualise the benefits to homophily and heterophily as the results of a simple coordination game. For example, homophily may yield fitness advantages because individuals using the same mode of communication may be able to act together more effectively. These advantages are sometimes called synergy. On the other hand, heterophily may be beneficial because it gives rise to specialisation or gains from trade, such as when a farmer interacts with a baker22, when different scientists collaborate23, or when individuals at different stages in the life cycle interact24.

We elaborate a simple model that assigns benefits to interactions and allows individuals to have preferences to interact with others with similar or different phenotypes. We then let these preferences co-evolve with the set of available phenotypes. This model shows that homophily emerges as the dominant preference under a wide variety of conditions.

For simplicity, suppose there is a haploid asexual population of size \( N \). There are \( M \) possible phenotypes (size, colour, behaviour, etc.), and each individual \( i \) has an observable phenotype denoted by \( G_i \). To be sure the phenotypes do not drive the results, we assume that none of these phenotypes alone make individuals more or less fit; only combinations of phenotypes between individuals determine fitness. When individuals \( i \) and \( j \) interact, they obtain a homophilic interaction payoff, \( a \), when they are of the same phenotype \( (G_i = G_j) \). We can
think of this as the payoff to synergy. When i and j are of different phenotypes \((G_i \neq G_j)\), they receive a heterophilic interaction payoff, \(b\); we can think of this as the payoff to specialisation. We assume that when individuals do not interact, their payoff is 0.

We can describe three kinds of environments from this basic set up. When \(a > b\) there is an advantage to homophilic interactions. When \(a < b\) there is an advantage to heterophilic interactions. Finally, when \(a = b\) there is no advantage to either homophily or heterophily.

At each time period, we assume there is a process that allows each individual to interact with another individual. This process proceeds in three stages, 1) choose, 2) meet, 3) interact. With probability \(p_i \in [0, 1]\), individuals will choose to interact with individuals of the same phenotype (homophily) and with probability \(1 - p_i\), they will choose to interact with individuals of different phenotypes (heterophily). Note that \(p_i = 1\) means that individual \(i\) always chooses individuals of the same phenotype and never of the opposite phenotype (perfect homophily). Conversely, \(p_i = 0\) means that individual \(i\) always chooses individuals of different phenotypes and never individuals of the same phenotype (perfect heterophily). And for intermediate values \(0 < p_i < 1\), individuals show a tendency to favour one kind of interaction over another. When \(p_i > 0.5\), then individual \(i\) tends to be homophilic, and when \(p_i < 0.5\), individual \(i\) tends to be heterophilic.

Next, individuals meet. For simplicity, we assume they are randomly paired with other members of the population (one can imagine more complex assumptions about meeting – we consider this possibility below). Once they meet, they interact, but only if both individuals have chosen to initiate an interaction with a partner that is compatible with their preferences and phenotypes. Hence, the probability of a successful interaction between two individuals \(i\) and \(j\) is \(p_i p_j\) if they are of the same phenotype \((G_i = G_j)\) and \((1 - p_i)(1 - p_j)\) if they are of different phenotypes \((G_i \neq G_j)\).

### Results

One advantage of conceptualising homophily in this way is that we can estimate the average homophilic preference \(p\) for several species and phenotypes in a number of available data sets (Table 1; see also SI) assuming that observed interactions are successful matches. Note that these real world observations show that homophily \((p > 0.5)\) is apparent in all cases, with the estimated value ranging between 0.53 and 0.68.

| Species                        | Phenotype | Mean homophilic preference | SE     |
|--------------------------------|-----------|---------------------------|--------|
| Humans (adults, U.S.)          | sex       | 0.68                      | 3 × 10^{-11}|
|                                | age       | 0.67                      | 4 × 10^{-4}|
| Humans (children, U.S.)        | sex       | 0.54                      | 3 × 10^{-12}|
|                                | race      | 0.65                      | 1 × 10^{-5}|
| Humans (adults and children, India) | race     | 0.68                      | 8 × 10^{-5}|
|                                | age       | 0.59                      | 8 × 10^{-12}|
| Dolphins                       | sex       | 0.60                      | 1 × 10^{-4}|
| Colobus monkeys                | sex       | 0.66                      | 2 × 10^{-10}|
| Zebras                         | sex       | 0.66                      | 1 × 10^{-10}|

We assume fitness is an exponential function of payoffs\(^{24}\), and individuals reproduce proportional to their fitness according to a frequency-dependent Moran process\(^{24}\), which can occur either via natural selection (the less fit die and are replaced by the more fit) or learning (the less fit copy the preferences of the more fit)\(^{25-29}\). We also allow for mutation. The probability that an offspring changes at random to one of the M phenotypes (each with equal likelihood) is \(\nu\), and in expectation \(v = \nu N\) offspring will change. Similarly, the probability that an offspring changes to a preference drawn from a uniform distribution with support \([0, 1]\) is \(u\), with \(\mu = uN\) offspring changing in expectation. For full details of the model, please refer to the SI.

Before discussing the equilibria of the model, we use a simple example to provide an intuition for why there is an advantage to homophily. Suppose there are \(N_1\) individuals in group 1 with phenotype 1 and \(N_2\) in group 2 with phenotype 2. Further suppose that all individuals within each group have the same preference \((p_1, p_2, \ldots, p_M)\), respectively. The payoff to an individual in group 1 is then \(a(N_1 - 1)p_1^2 + bN_2(1 - p_1)(1 - p_2)/(N_1 - 1)\), where \(N = N_1 + N_2\). Taking two extreme cases, perfect homophilic preferences \((p_1 = 1)\) and perfect heterophilic preferences \((p_1 = 0)\), we can see that homophilic preferences yield a payoff advantage to individuals in group 1 if \(a > bN_2(1 - p_2)/N_1 - 1)\). Remarkably, this equation shows that homophily pays even if the benefit, \(a\), to same type interactions is lower than the benefit, \(b\), to opposite type interactions. This happens when group 1 is in the majority (it is easier to connect to a similar phenotype individual in a larger group) and/or when group 2 is also homophilic (which reduces the payoff to heterophilic interactions).

Using coalescent theory\(^{30}\), we derive a closed-form solution for the limiting distribution of the preferences that survive in the population at equilibrium\(^{31,32}\), and we replicate all predictions with computational simulations. Figure 1 shows an example of three such equilibria.

When the payoff to homophilic interactions is high, those with a preference for homophily (high \(p\)) are more common than those with a preference for heterophily. Compared to a population with preferences distributed uniformly at random, the theory establishes a specific critical point \(p_c\) above which individuals are favoured and below which they are disfavoured by natural selection. When the benefit to interacting with similar and dissimilar others is more in balance, a bimodal distribution of preferences emerges with most individuals strongly preferring either homophilic or heterophilic interactions. Finally, when the payoff to specialisation is high, those with a preference for heterophily (low \(p\)) emerge and are favoured when they have a preference below a critical point \(p_c\).
While these results may seem unsurprising, Figure 2 shows that the theory generates an elegant critical threshold \( a > K b \) that determines whether the average individual in the population will evolve to become homophilic. The slope of this threshold is:

\[
K = \frac{v(\mu + v + 2)(M - 1)}{v(\mu + v + 2) + (\mu + 2v + 3)M}.
\]

where \( M \) is the number of possible phenotypes, and \( \mu \) and \( v \) are mutation rates that are rescaled by the population size \( N \), \( \mu = uN \) and \( v = vN \).

An important implication of this condition is that homophily can evolve even when the benefit \( b \) to heterophily (specialisation) exceeds the benefit \( a \) to homophily (synergy). This happens when \( K < 1 \). For example, Figure 2 shows that decreasing the number of phenotypes in the population \( M \), the phenotypic mutation rate \( v \), or the preference mutation rate \( \mu \), all decrease \( K \) and in turn increase the range of values under which homophily can emerge. Figure 3 shows that the average individual in the population becomes less homophilic as we increase each of these three parameters. And, in Figure 4, we show the full set of conditions under which homophily evolves for a given population size. We emphasise that homophily evolves even if \( a \ll b \) as long as the (phenotypic) mutation rates are sufficiently low.

We studied the behaviour of the critical point \( p_c \) (see SI) and found a surprisingly strong tendency toward homophily when mutation rates are low. In fact, when we let both \( v \) and \( \mu \) approach 0, the model shows that natural selection favours all individuals with \( p > 1/\sqrt{3} \). In other words, all homophilic individuals and even those individuals that weakly prefer heterophily tend to do better than those that strongly prefer heterophily. And this result is independent of the payoff to heterophilic interactions, \( b \), and phenotypic diversity, \( M \). The only requirement is that the payoff to homophilic interactions, \( a \), be positive.

Given constraints on mobility, it may be unrealistic to assume that individuals are equally likely to meet with all other members of the population. In many species (including humans) interactions tend to be more likely between individuals of the same type because they are drawn to and/or drawn from similar environments. We therefore extended the basic model by introducing an additional parameter to allow for such assortativity. With probability 0 < \( \phi < 1 \), individuals interact with others of the same phenotype, and with probability 1 - \( \phi \) they interact as before (see SI).

As it turns out, this extension generates an almost identical critical threshold, with homophily emerging when \( a > (1 - \phi)Kb \). Since \( \phi < 1 \), this result shows that any degree of assortative matching that brings similar types into contact with one another more often makes it even more likely that homophily will evolve.

Another strong assumption of the basic model is that increasing a preference to interact with individuals of the same phenotype \( (p) \) yields an equal and opposite decrease in the preference to interact with individuals of different phenotypes \( (1 - p) \). Yet some individuals might want to interact with both similar and different phenotypes. We relaxed this assumption by allowing a separate preference \( q \) (independent of the preference \( p \)) to evolve that indicates the probability that an individual interacts with individuals of different phenotypes. Thus, each individual was characterised by a triplet \( \{G_i, p_i, q_i\} \) denoting phenotype, homophilic preference, and heterophilic preference, respectively.

In this extended version of the model (see SI), we found that the average homophilic preference \( (p) \) was greater than the average het-
erophilic preference \( \langle q \rangle \) in equilibrium if and only if \( a > Kb \). Note that this is exactly the same condition that results from the basic model. Moreover, under the same condition \( (a > Kb) \), the population consists of more homophilic individuals \( (p > q) \) than the counterpart, heterophilic ones \( (p < q) \). In other words, the population tends to show more homophily than heterophily.

Finally, in all models, we assume natural selection is weak, which means that fitness differences are very small. Increasing the strength of natural selection relaxes this assumption and magnifies the fitness difference between traits. As a result, the evolutionary dynamics become increasingly deterministic, and the critical point \( p_c \) and the distribution of preferences in equilibrium become more skewed towards the extremes \( (p = 0 \) and \( p = 1) \).

**Discussion**

Our model differs from these prior studies that have taken into account assortativity in mating choice or ecological competition interactions. Among them, one study\(^4\) concerns whether a particular assortative mating choice of females is favoured for a fixed composition of phenotypes in the population. In this model, the mating choice is exclusively unilateral and up to females, and the derived condition only gives the direction of the evolution at a given
population composition. In contrast, interactions in our model are based on bilateral agreement, individuals’ preferences and phenotypes are allowed to co-evolve, and most importantly, the mutation-selection equilibrium is analytically derived that explicitly accounts for the abundance of any homophilic trait in the long run evolution. Some other previous studies, for example, consider the role of pre-existing assortative competition, but rather than the emergence of assortativity per se, in asexual or sexual selection contexts. Complementing and strengthening these prior works, our model here explicitly addresses how homophily evolves in the first place. Furthermore, our evolutionary model shows how homophily can emerge under a wide variety of conditions, particularly when mutation rates are low. It is not surprising that the payoff to homophilic interactions must be high relative to the payoff to heterophilic interactions in order for homophily to evolve. However, the analysis also suggests that this relationship is only relative, since the threshold for the ratio between these benefits can be less than one. This means that synergy may have a powerful effect on evolution, even when there are substantial benefits to specialization, helping to drive alternative phenotypes to extinction. In higher-order species, the emergence of language or other forms of communication, or of certain cognitive capacities, might serve such a function, and may help to promote a general tendency to seek out similar individuals with whom to cooperate or interact.

The model also shows that even small advantages to synergy can significantly reduce phenotypic diversity. Heterophilic populations maintain diversity by privileging rare phenotypes, generally causing their distribution to become uniform. Homophilic populations, on the other hand, privilege common phenotypes, helping to drive alternative phenotypes to extinction. Even if all phenotypes are themselves fitness neutral (as they are in our model), advantages to synergy will tend to yield populations dominated by a single phenotype, and in the long run the population will tend to oscillate from one dominant phenotype to another, with rapid phase transitions in between.

Our results may also shed light on the observation that evolution in humans is accelerating. The human capacity to collaborate not only with kin but also with unrelated members of our species may have dramatically increased the potential gains from synergy, and this shift in payoffs would not only favour interactions with similar partners, but would also affect the overall desire to search out such partners. A wide variety of studies suggest that humans particularly seek out similar others, even when there are no obvious benefits to these interactions (on the contrary, there may be more benefits to specialisation). Hence, it is possible that we evolved a strong predilection for homophily once we started to interact frequently with unrelated individuals. Such an effect would especially accelerate the evolution of phenotypes that are intrinsically synergistic, such as those related to communication or other collaborative activities.

Here, we focus on only one phenotypic dimension, but it is possible to extend our model to multiple dimensions of phenotypes (see SI). Payoffs to synergy and specialisation may vary for different sets of phenotypes, as each set serves a different function in social interactions. Therefore, multi-layer networks superimposed on various types of social interactions could result, and each layer could play a different role. It is possible that in one layer ‘similarity attracts’, leading to stable, long-term relationships, while in another layer
‘opposite attracts’, which often results in short-lived task-related ties’. In this way, natural selection could lead to the delicate, if very lopsided, balance between homophily and heterophily that we observe today in the real world.

Methods
In the Supplementary Information, we elaborate on the model presented above and analyse it, characterising equilibria under mutation-selection, explaining selection criteria, deriving a formula for continuous preferences, and showing long form equations for the triplet correlations at neutrality that allow us to use coalescent theory to derive conditions for the evolution of homophily. We then describe how we derived the critical slopes and critical preferences shown in the main text, and characterise equilibria for the whole parameter space. Finally, we turn our attention to several extensions of the model, analytically characterising models with biased matching, local mutation, strong selection, full strategy space, and multiple sets of phenotypes.

We also describe the application of the model to derive estimates of homophily from empirical data, as shown in Table 1.

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F.E., M.A.N., N.A.C. and J.H.F. performed analyses, discussed the results, and contributed to the text of the manuscript.

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