Multi-quasiparticle sub-nanosecond isomers in $^{178}$W

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A B S T R A C T

We report on the first measurement of the half-lives of $K^π = 11^−$ and $12^+\,$ four-quasiparticle states in the even-even nucleus $^{178}$W. The sub-nanosecond half-lives were measured by applying the centroid shift method to data taken with LaBr₃(Ce) scintillator detectors of the NuBall array at the ALTO facility in Orsay, France. The half-lives of these states only became experimentally accessible by the combination of several experimental techniques - scintillator fast timing, isomer spectroscopy with a pulsed beam, and the event-by-event caloriometry information provided by the NuBall array. The measured half-lives are 476(44) ps and 275(65) ps for the $I^\pi = 11^−$ and $12^+$ states, respectively. The decay transitions include weakly hindered $E1$ and $E2$ branches directly to the ground-state band, bypassing the two-quasiparticle states. This is the first such observation for an $E1$ transition. The interpretation of the small hindrance hinges on mixing between the ground-state band and the $t$-band.

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1. Introduction

The A ≈ 180 region of deformed nuclei exemplifies the competition between individual-particle and collective degrees of freedom [1]. A key aspect is that the projection of the angular momentum, K, on the nuclear symmetry axis is approximately conserved, and this gives rise to K isomers when the change in K-value, $ΔK$, exceeds the multipole order of the decay radiation, λ. Such transitions are called “K-forbidden”, and the degree of forbiddenness is defined as $ν = ΔK - λ$. An extreme case is the $T_{1/2} = 31\,$ y, $K^π = 16^+$ isomer in $^{178}$Hf at an excitation energy of 2446 keV [2], which is 989 keV below the $K = 0$, $I^\pi = 16^+$ collective rotation of the ground-state band (CSB). The 31-y isomer has a structure based on two broken nucleon pairs, i.e. it is a four-quasiparticle (4qp) state.

However, the competition between individual-particle and collective excitations changes quickly with nucleon number. In $^{178}$W, for example, with two more protons and two fewer neutrons, the longest-lived 4qp state ($K^π = 15^+$) observed to date has a half-life...
of just 30 ns, and there are other 4qp states (e.g., \( K^\pi = 11^- \) and \( 12^+ \)) with half-lives that have been too short to measure in previous studies (\( T_{1/2} \leq 2 \) ns and \( \leq 1 \) ns, respectively) [3]. Furthermore, these two states lie at excitation energies considerably above the yrast line (the \( 12^+ \) state is 991 keV above the \( 12^+ \) GSB member) and they have highly \( K \)-forbidden decay branches directly to the GSB, bypassing the 2qp states. The bypassing transitions demonstrate an apparent collapse of the goodness of the \( K \) quantum number, thus providing extreme examples of so-called “anomalous” decays that were first identified from the 6qp, \( T_{1/2} = 130 \) ns isomer in \(^{182}\text{Os} \) [4], and the 4qp, \( T_{1/2} = 5.7 \) \( \mu \)s isomer in \(^{144}\text{Hf} \) [5].

It has been a long-standing experimental challenge to measure the short half-lives of the \( K^\pi = 11^- \) and \( 12^+ \) states in \(^{178}\text{W} \), so that the extreme nature of their anomalous decays can be quantified. Hence, it would be possible to understand better the way in which the \( K \) quantum number is broken down. However, the level structure of \(^{178}\text{W} \) and its \( \gamma \)-ray spectra are complex, and the non-yrast location of the 4qp states leads to weak population. Nevertheless, as we now report, by exploiting a pulsed beam and a reaction that populates higher-lying isomers, together with an array of \( \text{LaBr}_3(\text{Ce}) \) detectors combined with Ge detectors, and advanced analysis techniques, it has been possible to measure the half-lives of these states.

2. Experimental conditions

The experiment was performed at the ALTO accelerator facility at the IPN Orsay, France. A beam of \(^{16}\text{O} \) ions was impinged on a 6.3 mg/cm\(^2 \) target of enriched \(^{164}\text{Dy} \) with a 1 mg/cm\(^2 \) Au backing. The beam consisted of bunched 2 ns long pulses with 400 ns repetition period. The strongest channels were \(^{164}\text{Dy} \to ^{180}\text{Os} + 4\alpha\) \(^{178}\text{W} \) and Coulomb excitation of the target nucleus. During the six-day measurement about equal time was used for three different beam energies, 71 MeV, 76 MeV, and 80 MeV. The Coulomb barrier lies at 72 MeV. The data taken with the beam energy at 71 MeV were not included in the current analysis.

Decay \( \gamma \) radiation was detected with the NuBall array [6] which was set up for a long campaign at Orsay that lasted from November 2017 until late summer of 2018. The array consisted of 24 Clover detectors close to 90 degrees with respect to the beam axis. There were 10 co-axial HPGe detectors at backward angles, and 20 \( \text{LaBr}_3(\text{Ce}) \) detectors at forward angles.

Data acquisition was fully digital and implemented with the \textit{“FASTER”} system [7]. The \( \gamma - \gamma \) time resolution (FWHM) of the Ge and \( \text{LaBr}_3 \) detectors, measured with a \(^{60}\text{Co} \) source, was 20 ns and 320 ps respectively. This was the first experiment of the NuBall campaign. The detector and electronics setup was slightly different with respect to the later measurements with the LICORNE neutron source [8]. The differences shall briefly be highlighted here. There were two categories of \( \text{LaBr}_3(\text{Ce}) \) crystals, 10 of truncated cone shape, 1.5” in length and 1” and 1.5” at the bases [9] and 10 of the UK \textit{FATIMA} type with cylindrical shape and dimensions 1.5” \times 2” [10], both using the same R9779 photo multiplier tube (PMT) from Hamamatsu. The conical detectors had a 1 mm layer of lead shielding around the crystal. No other shielding was present between the \( \text{LaBr}_3 \) detectors. Only the \( \text{LaBr}_3 \) detector channels in the data acquisition had a digital CFD for time walk minimisation and sub-nanosecond time pick-off. This means that walk correction for Ge and BGO detectors was performed offline. For the \( \text{LaBr}_3 \) detectors a residual time wall correction (on the picosecond scale) was applied offline (see below). In contrast to later experiments in the campaign a global trigger was used. The trigger condition was (one \( \text{LaBr}_3 \) AND one Ge) OR (two \( \text{LaBr}_3 \)) detectors within a window of 2 \( \mu \)s.

In general conditions during the experiment were very stable. In particular we did not observe a significant gain drift in the \( \text{LaBr}_3 \) energy spectra during the measurements with each individual beam energy. However, we observed gain shifts between the different energy runs, which we attribute to different \( \gamma \)-ray rates.

3. Data analysis and results

The aim of this analysis was to obtain the lifetimes of short-lived sub-nanosecond isomers in \(^{178}\text{W} \). From previous measurements using Ge detectors some of these levels were known to have lifetimes shorter than a couple of nanoseconds [3,11]. The better time resolution of \( \text{LaBr}_3(\text{Ce}) \) scintillator detectors makes a delayed \( \gamma - \gamma \) coincidence lifetime measurement using the centroid shift method [12] possible. This method is well established and based on the fact that the centroid \( C \) of a delayed time distribution is shifted with respect to that of a corresponding prompt time distribution \( C_{\text{Prompt}} \) by the mean lifetime \( \tau \) of the intermediate state:

\[
C = C_{\text{Prompt}} = \tau.
\]

Measurements with \(^{60}\text{Co} \) and \(^{152}\text{Eu} \) sources were used for energy, efficiency, and timing calibration. The precise determination of the residual prompt response time walk for the \( \text{LaBr}_3 \) detectors is crucial for sub-nanosecond lifetime measurements with the centroid shift method [13]. By measuring previously reported lifetimes in \(^{164}\text{Dy} \) it was demonstrated that the calibration taken with the \(^{152}\text{Eu} \) source holds under in-beam conditions [14]. The same publication [14] contains a figure of the prompt response timewalk \( C_{\text{Prompt}}(E_\gamma) \) which was used in this work.

Coincidences between neighbouring detectors, which are dominated by Compton scattering between crystals, were excluded from the analysis.

The study of the decay of long-lived isomers in \(^{178}\text{W} \) is facilitated through the pulsed beam. This allows the selection of \( \gamma \) rays that are emitted after population of long-lived isomers, of which there are several at energies above 3 MeV in \(^{178}\text{W} \), e.g., the 15^- state at 3654 keV with \( T_{1/2} = 30 \) ns or the 21^- state at 5314 keV with \( T_{1/2} = 64 \) ns [3]. By selecting \( \gamma \) rays that were emitted outside of the prompt time region around a beam pulse, the coincidence spectra can be cleaned up significantly. In this way it is possible to perform \( \gamma - \gamma \) delayed coincidence measurements out of beam. Doing this with the \( \text{LaBr}_3 \) detectors enables us to measure the lifetime of short lived isomers in these very complex excitation spectra for the first time. Statistics was not sufficient to allow an additional energy gate on the Ge detectors.

One significant feature of the NuBall array is the fact that the BGO crystals surrounding the Ge detectors were not shielded towards the target position. The intention of this was to use them as an additional source of information for calorimetry studies. In an analysis like the present one it can be used as a powerful channel selection tool, as it provides us with a high-efficiency multiplicity filter. By setting conditions on the number of detected \( \gamma \)-rays for both the prompt and delayed part of an event, we were able to improve the peak-to-background ratio of our transitions of interest by a factor of up to 3.5, while at the same time reducing the total number of counts in the coincidence spectra only by a factor of about 2. The delayed time window was set from 40 ns to 270 ns after the beam pulse.

In our case the condition of prompt multiplicity \( \geq 1 \) and delayed multiplicity \( \geq 3 \) was found to be a good compromise between statistics and peak-to-background ratio for the study of the short lived isomers around 3 MeV in \(^{178}\text{W} \).
With these conditions we identified two isomers whose lifetimes we were able to measure. Attempts to measure the lifetimes of other high-lying states, like the 18$^\text{−}$ state at 4878 keV, or those of the states in the band of the 13$^\text{−}$ level at 3523 keV were unfortunately not successful due to low statistics or contaminations.

We were able to set clean LaBr$_3$ energy gates on transitions populating and de-populating the 11$^\text{−}$ isomer at 3053 keV, namely the $\gamma$ cascades 181 keV - 921 keV and 181 keV - 1090 keV. See Fig. 1 for a partial level scheme of $^{178}\text{W}$.

The lifetime of the 12$^+$/isomer at 3235 keV was not accessible in this direct way. Cating on the 290 keV transition, the peak of the coincident transition at 181 keV - connecting the state at 3235 keV with the state at 3053 keV - is contaminated significantly with a $\gamma$ ray at energy 184 keV. These two transitions cannot be resolved in the LaBr$_3$ spectrum, which renders a direct coincidence measurement of this state’s lifetime impossible in this case. Therefore, we took advantage of a general feature of the centroid shift method that has mainly been exploited in $\beta$-$\gamma$ fast timing measurements before [12]. If the time difference spectrum of two transitions in a direct cascade going through states with lifetimes $\tau_1$, $\tau_2$, etc., is measured, then the centroid $C^*$ of this coincidence is actually shifted by just the sum of the lifetimes of the intermediate states

$$C^* = C - C_{\text{Prompt}} = \tau_1 + \tau_2 + ...$$

(1)

The coincidence cascade 290 keV - 921 keV is clean, and the same is true for 290 keV - 1090 keV. As we have already determined the lifetime of the 11$^\text{−}$ state directly we can infer the lifetime of the 12$^+$ state using these coincidences via the above mentioned relation.

As can be seen from Figs. 2 and 3 there is still significant coincidence background - stemming mostly from Compton scattered coincident $\gamma$ rays – which has to be treated accordingly. The peak-to-background ratio is 0.63 for Fig. 2 a, and 0.76 for Fig. 3 b). In all lifetime measurements in this work we applied the procedure described in ref. [15], where the background contribution to the centroid of the total time spectrum is separated into three parts. These are then individually estimated by setting energy gates outside of the coincidence region and interpolating the value at the peak position. Polynomial functions were used for interpolation, and the uncertainty was in each case estimated from the standard deviation of the fit residual. The centroid position for the full energy peak coincidence is then obtained by subtracting the background centroids with the appropriate weights from the total distribution. One advantage of this approach is that no assumptions about the shape of the background time distributions have to be made.

With this background corrected centroid value the lifetime can then be determined by applying the prompt response correction, which was obtained from the $^{152}\text{Eu}$ calibration [14]. The results for the individual measurements are given in Table 1. The contribution of the prompt response correction to the uncertainty of the lifetime is of the order of 10 ps (7 ps for the half-life).

From the results in Table 1 we calculated a weighted mean for both lifetimes. The half-lives are 476(44) ps and 275(65) ps for the 11$^\text{−}$ and 12$^+$ isomers (Table 2), respectively. While these are short compared to typical K isomers, they at least indicate that intrinsic (quasiparticle) states are involved, and it is reasonable to assign the K values as being equal to the spin values. Relative $\gamma$ intensities were measured using the Ge detectors. Conversion coefficients were calculated using the Brice code [16]. The obtained reduced hindrance factors $f_v$ for the transitions depopulating the 3235 keV and 3053 keV levels are shown in Tables 3 and 4. Here, $f_v$ is defined as the $v$th root of the Weisskopf hindrance factor [1,2]. Note also that the assumption of pure multipoles is for the purpose of evaluating conversion coefficients and $f_v$ values. In the case of M1 transitions, significant E2 admixtures are possible, but these have not been measured. In fact, for the present data, the $f_v$ values for the other transitions, i.e. E1 and stretched E2, are not affected (within error bars) by this assumption.
4. Discussion

4.1. The low E2 hindrance from the 12+ isomer to the GSB

The variation of reduced hindrance with proton number is shown in Fig. 4. The figure includes all E1 and E2 “bypassing” transitions from 4qp isomers in even-even nuclides, directly to the GSB, i.e. bypassing the 2qp states. The general trend of decreasing $f_\nu$ with increasing Z could be due to increasing gamma softness [1,2]. Nevertheless, it is evident that all the values are low ($f_\nu < 6$). Here the focus is on the $^{178}$W value, which is even lower than might be expected from the trend of the data, but first we recall the situation for $^{174}$Hf.

The $^{174}$Hf value was discussed [5] in terms of mixing with an isolated $(i_{13/2})^2$ s-band state at $I=12$, though now it would be more appropriate to give a t-band interpretation (where the Fermi-aligned $i_{13/2}$ neutrons have significant K projections – see [17] for a recent summary of t-band structures). Either way, when the high-K structure of the $(i_{13/2})^2$ admixture is not explicitly taken into account, there is the appearance of low reduced hindrance for the E2 decay to the GSB.

In a similar way, there is t-band mixing in $^{178}$W [3]. Importantly, in this case the yrast (energetically unfavoured) band for $I \geq 12$ has been identified as a t-band with $K \approx 8$. The high-K value was extracted by Purry et al. [3] from an analysis of the E2 branching ratios in the crossing region with the GSB, and a GSB/t-band mixing matrix element of 68 keV was obtained. Although the $I=10$ member of the t-band was not assigned, this could plausibly be the $I^T = 10^+$ state at 2682 keV, which is fed from the K$^\pi = 12^+$ isomer by a 552 keV, E2 transition. If the 2682 keV state has K = 8 from the $(i_{13/2})^2$, $(\gamma^+ [633], \gamma^- [624])$ t-band coupling, then the 552 keV transition has $\nu = 2$, and $f_\nu = 4.3$. This is already a low value, but we note that the configuration of the $12^+$ isomer itself involves two $i_{13/2}$ neutrons $[3^+ [633], 9^+ [624]]$ coupled...
to $K = 8$ [3, 18], which is just the $t$-configuration, so that the decay to the 2682 keV level would require only a simple recoupling of the two other neutrons in the 4qp configuration.

Using the 68 keV mixing matrix element obtained by Purry et al. [3], the $10^+ \text{ GS}$ member at 1665 keV can be calculated in a two-level-mixing scenario to have a 0.5% $t$-band, $<K> \approx 8$ admixture. If that 0.5% component accounts for the observed 1571 keV transition from the $12^+$ isomer to the GS, but the reduced hindrance is calculated with $K = 0$ for the GS (as would usually be done) then an apparent reduced hindrance of $f_r = 2.3$ is predicted, which is exactly the observed value. While there are uncertainties in the assumptions used, the general understanding appears to be good: there is a small $t$-band admixture in the GS, which enables the direct transition to proceed from the $12^+$ isomer, and this transition may be facilitated by the particular structure of the 4qp isomer, which includes the 2qp, $t$-band configuration. Note that in the $^{174}$Hf case, there is no experimental evidence for the $K$ value of the $I = 12$ mixing state. Therefore the present case of $^{178}$W, with $K \approx 8$ for the $t$-band consistent with $E2$ branching ratios [3], has special significance for understanding the nature of bypassing transitions.

It would be desirable to apply the same procedure with the other 4qp isomers that have bypassing decays, i.e. those illustrated in Fig. 4. However, for $^{164}$Er [19], $^{174}$W [20] and $^{182}$Os [4], there are no observed $E2$ decay branches to the corresponding yrare states, so that a different kind of analysis would be required, involving different assumptions. From an experimental perspective, it would be valuable to identify these missing transitions.

Note also that the 991 keV, $\Delta I = 0$ transition to the $12^+$ member of the $^{178}$W GS also has a very low reduced hindrance, $f_r = 3.1$, assuming M1 character. This is slightly larger than for the competing $E2$ transition to the $10^+$ GS member, with $f_r = 2.3$. Such a difference between competing M1 and $E2$-forbidden decays is typical [2], but a quantitative discussion of the difference is inhibited by the lack of knowledge of the $E2/M1$ mixing ratio of the $\Delta I = 0$ transition.

4.2. The low $E1$ hindrance from the $11^-$ isomer to the GS

The $E1$ reduced hindrance, from the $11^-$ isomer directly to the $10^+$ member of the GS, $f_r = 2.8$, is very small – indeed, it is the smallest value yet observed for any $K$-forbidden $E1$ transition, and it is the only example of a bypassing $E1$ transition to the GS in an even-even nuclide. With the commonly employed $10^4$ reduction applied to the E1 Weisskopf hindrance factor [23, 24], similar $E2$ and (effective) $E1$ reduced hindrances are typically found, and this is certainly supported by the presently obtained values of $f_r = 2.3$ and 2.8, respectively.

The $11^-$ isomer configuration involves the $9^+_2$ [624], $i_{13/2}$ neutron [3, 18], but not both the $i_{13/2}$ neutrons of the $t$-configuration, as is evident for the $12^+$ isomer. Nevertheless, the same $t$-band mixing at $I = 10$ introduces high-$K$ components into the GSB $10^+$ state, which can account for the small apparent $f_r$ value for the $E1$ transition (though a quantitative evaluation of the reduced hindrance would require additional assumptions).

Finally, it is appropriate to consider whether there could be chance near-degeneracies involved, with states having the same spin and parity, but different $K$ values. Suffice to say that, at least for the $12^+$ and $11^-$ isomers, and the $10^+$ GS state, no such accidental degeneracies are known within an energy interval of 100 keV. However, with the two isomers being well above the yrast line, it remains a possibility that mixing with as-yet unobserved states could play a role.

5. Conclusion

With $\gamma$-ray fast-timing techniques, short half-lives have been obtained for $K^T = 11^-$ (0.48 ns) and $12^+$ (0.28 ns) 4qp states in $^{178}$W, at excitation energies close to 3 MeV. Their highly $K$-forbidden decays directly to the $10^+$ member of the GSB, bypassing the 2qp states, have very small reduced hindrance factors. These are interpreted as being at least partly due to mixing between the $10^+$ GSB member and the $10^+$ $t$-band state, which has a high-$K$ structure based on two $i_{13/2}$ Fermi-aligned neutrons. The $E2$ result ($f_r = 2.3$) can be understood in a similar way to the long-standing value in $^{174}$Hf, while the remarkably similar $E1$ result ($f_r = 2.8$) is a unique observation of its kind. Further experimental information is needed to enable a quantitative comparison of the $K$-mixing mechanism for bypassing decays in $^{164}$Er, $^{174}$W and $^{182}$Os. In the meantime, the present work provides some of the best evidence to date that high-$K$ admixtures in the GSB are key to understanding the apparent breakdown of the K quantum number.

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