Theoretical design of stable hydride clusters: isoelectronic transformation in the $E_nAl_{4-n}H_{7+n}^{-}$ series†

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New stable hydrogen-rich metallic hydrides are designed by systematic transformations of the stable known $Al_4H_7^-$ species, carried out by successive isoelectronic substitutions of one aluminum atom by one E–H unit at a time (where E = Be, Mg, Ca, Sr and Ba atoms). Searches on the potential energy surfaces (PESs) of $EAl_2H_9^-$, $E_2Al_2H_9^-$, $E_2AlH_{10}^-$ and $E_4H_{12}^-$ systems indicate that structural analogues of $Al_4H_7^-$ become higher energy isomers as the number of E–H units increases. The electronic descriptors: Vertical Electron Affinity (VEA), Vertical Ionization Potential (VIP) and the HOMO–LUMO gap, suggest that the systems composed of $EAl_2H_9^-$, $E_2Al_2H_9^-$, $E_2AlH_{10}^-$, with E = Be and Mg, would be the most stable clusters. Additionally, for a practical application, we found that the Be–H and Mg–H substitutions increase the hydrogen weight percentage (wt%) in the clusters, compared with the isoelectronic analogue $Al_4H_7^-$. The good capacity of beryllium and magnesium to stabilize the extra hydrogen atoms is supported by the increment of the bridge-like E–H–Al, 3center–2electron chemical bonds. Finally, explorations on the PESs of the neutral species (using Na⁺ as counterion) indicate that the NaBe$_2$Al$_2$H$_9$, NaBe$_2$AlH$_{10}$ and NaMgAlH$_{10}$ minimum-energy structures retain the original geometric shapes of the anionic systems. This analysis supports the potential use of these species as building blocks for cluster-assembled hydrides in the gas phase.

1. Introduction

The assembly of nanostructured materials using atomic clusters as building blocks is one of the most challenging procedures for the design of new substances with desired specific properties. This happens because when going from cluster to the assembled material, the physical and chemical properties may vary greatly. For this reason, finding stable enough atomic clusters with particular properties is a key step. Among the possible building blocks, aluminum hydrides have received considerable attention due to their high hydrogen content, making them suitable building blocks for potential hydrogen storage materials. Experimental and theoretical studies on the closo-alanes series established that the most stable configurations are composed of a polyhedral arrangement, in which the high stability is explained by Wade’s rule. Likewise, experimental and theoretical studies about the $Al_4H_{m-n}^-$ series revealed that the $Al_4H_7^-$ composition has an exceptional stability and low reactivity. This is rationalized in terms of the Jellium model; the $Al_4H_7^-$ species is a closed shell system that contains 20 valence electrons reaching the magic number required by this model. Additionally, the authors proposed that if an alkali atom is added, to donate the charge, this complex could be used as a potential building block to form cluster-assembled hydrides. They found that the tetrahedral-like most stable $Al_4H_7^-$ structure is effectively conserved in the presence of a counterion (Fig. 1).

![Fig. 1. Lowest energy structures for $Al_4H_7^-$ and LiAl$H_7$ systems.](10.1039/c7ra01422h)

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A simple yet effective strategy for the theoretical design of new atomic clusters, with enhancing chemical and physical properties, is by replacing one fragment on a well-known stable species by another isoelectronic one (i.e. by an atomic or molecular unity containing the same number valence electrons). One example of this design strategy is presented in the AlB2H6, AlB2H12 and AlB2H13 aluminoboranes compounds, where one B of stable boranes is replaced by one Al, which have triggered considerable attention of the worldwide hydrogen storage research community. Recently, we have established an isolobal analogy between the B–H or the Al–H unit and the silicon atom in a series of theoretically designed stable deltahedral compounds. The transformation from Si52– to B3H62– or Al3H62– has been made possible by successive isoelectronic substitutions of silicon atoms by B of stable boranes is replaced by one Al, which have triggered considerable attention of the worldwide hydrogen storage research community. Recently, we have established an isolobal analogy between the B–H or the Al–H unit and the silicon atom in a series of theoretically designed stable deltahedral compounds. The exceptional stability of Al4H7– system leads us to the following question: What would be the impact of replacing aluminum atoms by E–H units (E = Be, Mg, Ca, Sr and Ba) on both the stability and the structure of the resulting system? Theoretically, the new systems should contain more hydrogen per unit cluster. The well-known fact that of group 2 elements in the periodic table, especially beryllium and magnesium, are good hydrogen retainers, justifies the possibility of improving the hydrogen storage capability on the systems to be designed. This hypothesis is verified by our theoretical results. Additionally, the resulting most stable structures are also stable in the presence of one counterion, thus enabling their use as building blocks for assembling nanostructured materials for hydrogen storage purposes.

2. Computational details

An unbiased exploration of PESs for the EAl3H8–, E2Al2H9–, E3AlH10– and E2H11– (E = Be, Mg, Ca, Sr and Ba) systems, in both, singlet and triplet electronic states, was conducted using the gradient embedded genetic algorithm (GEGA). All GEGA calculations were done using the PBE0 (ref. 23 and 24) hybrid density functional in conjunction with the Stuttgart–Dresden pseudopotentials and their respective basis set (SDD). The}

\[
BE = \frac{nE(E^0) + (4 - n - 1)E(AI^0) + 1E(Al^-) + (7 - n)E(H^0) - E(E_{nAl_{6-n}H_{7+n}}^-)}{n + (4 - n) + (7 + n)}
\]

building blocks for assembling nanostructured materials for hydrogen storage purposes.

where \(E(E^0), E(AI^0), E(Al^-)\) and \(E(H^0)\) correspond to the energies of (E = Be, Mg, Ca, Sr and Ba), Al, Al– and H atoms, respectively, and \(E(E_{nAl_{6-n}H_{7+n}}^-)\) is the energy of each cluster. The chemical bonding analysis of the lowest energy isomers were performed using the Adaptive Natural Density Partitioning (AdNDP) method, which was developed and written by Zubarev and Boldyrev. This approach leads to the partitioning of the charge density into elements with the lowest possible number of atomic centers per electron pair: \(n\) center-two electrons (\(n\)–2e), including core electrons, lone pairs, 2c–2e bonds, and so on. All calculations were carried out utilizing the Gaussian 09 program.
the AdNDP surfaces were drawn with Chemcraft 1.6 (ref. 35) and Molekel 5.4,36 respectively. Finally, we performed GEGA searches using sodium as counterion to obtain the alkali–clusters complexes.

3. Results and discussions

3.1 Global minima structures

The lowest energy structures obtained after GEGA and refining procedures for $E_n Al_{4-n} H_{7-n}$ systems, with $E = Be, Mg, Ca, Sr$ and $Ba$, and $n = 1–3$, are presented in Fig. 2.

Considering that the high-energy isomers could be stabilized under certain conditions (higher temperatures, chemical environment, or others), we also reported all the isomers (within the range of 10 kcal mol$^{-1}$ above the lowest energy one) found in the respective singlet PESs (Fig. SI-1 to SI-20†). The searches on the potential energy surfaces (PES) for the first substitution, one aluminum by one $E$–$H$ unit, located the $1E$-1 tetrahedral-like (analogue to the $Al_{4}H_{7}$ system) arrangements as global minima for $E = Mg, Ca$ and $Sr$. The situation was different for beryllium and barium-doped systems; the tetrahedral analogues were less stable than the corresponding global minima, the boat-shape $1Be$-1 and $1Ba$-1 structures, by 6.2 and 4.9 kcal mol$^{-1}$ respectively. We attribute these differences to the atomic size of beryllium and barium, which are more dissimilar with respect to aluminum than magnesium, calcium and strontium. For the substitution of two aluminum atoms by two $E$–$H$ units, the searches revealed the presence of the $2E$-1 tetrahedral analogues as the most stable configurations for $E = Mg, Ca, Sr$ and $Ba$. This was not the case for beryllium, in which the $2Be$-1 global minimum, a planar-like structure stabilized by the presence of a $Be$–$Be$ dimer, was more stable by 6.4 kcal mol$^{-1}$. The PESs exploration, for the systems obtained after three substitutions, showed that the tetrahedral analogue configurations, $3E$-2, were unstable for $E = Be, Ca, Sr$ and $Ba$. The only exception, the tetrahedral-like magnesium doped system, was found at 1.2 kcal mol$^{-1}$ above the $3E$-1 global minima. The similarity in the atomic size between aluminum and magnesium atoms could explain the stability of this $3Mg$-2 tetrahedral analogue.
Instead, the \( \text{AlH}_4^- \) portion and the presence of an \( \text{E}_3 \) triangle, a fragment capable of incorporating six hydrogen atoms, characterize the \( 3\text{E}-1 \) global minima structures. Finally, the global minima structures for the total substitutions of the aluminum atoms by \( \text{E}^- \) units are shown in Fig. 3.

Dissociated forms (consisting of a hydrogen molecule and \( \text{E}_4\text{H}_5^- \) clusters) constitute the most stable configurations. This means that the storage of the maximum number of hydrogen atoms in a compact and stable structure by total aluminum replacement is not possible. At this point, we can conclude that systems substituted with one, two and three \( \text{E}^- \) units were able to generate compact hydrogenated configurations. Remarkably, analogues to \( \text{Al}_4\text{H}_7^- \) (\( \text{EA}_3\text{H}_8^- \) (\( 1\text{E}-1 \), \( \text{E}^- \) = Mg, Ca and Sr), \( \text{E}_2\text{Al}_2\text{H}_9^- \) (\( 2\text{E}-1 \), \( \text{E}^- \) = Mg, Ca, Sr and Ba) and \( \text{E}_3\text{AlH}_{10}^- \) (\( 3\text{E}-1 \), \( \text{E}^- \) = Mg) series) adopt tetrahedral-like structures.

In order to postulate possible candidates as building blocks to assemble structures, our next objective is to explore relative kinetic and thermodynamic stability tendencies among the found global minima. Some energy descriptors, such as Vertical Electronic Affinity (VEA), Vertical Ionization Potential (VIP) and HOMO–LUMO gap, can help to evaluate these relative reactivity tendencies. Likewise, relative Binding Energies (BEs) provide us with a picture about relative thermodynamic stabilities.

### 3.2 Relative stabilities

Global reactivity descriptors and BEs tendencies for the global energy minima structures of \( \text{EA}_3\text{H}_8^- \), \( \text{E}_2\text{Al}_2\text{H}_9^- \) and \( \text{E}_3\text{AlH}_{10}^- \) series are presented in the Fig. 4.

According to VEA values, systems substituted with one, two and three \( \text{Be}^- \)-H and \( \text{Mg}^- \)-H units, display the highest...
capacity to stabilize an extra negative charge in the geometry of the mono-anion, even higher than the Al₄H₇⁻ cluster (dashed lines in Fig. 4). On the other hand, the VIP descriptor shows that systems substituted with three E–H units, with E = Be and Mg, present the highest resistance to be ionized. Similarly, according to the maximum hardness principle, the same systems showed the lowest reactivity, i.e., the highest HOMO–LUMO gap (see Fig. 4), and therefore, the highest hardness. In fact, the systems doped with two and three E–H units, with E from Be to Sr, are less reactive than the Al₄H₇⁻ cluster. Finally, the binding energy per atom, a thermodynamic stability descriptor, shows that the systems doped with Be–H units exhibit the highest stability.

The values reported in the Table 1 show similarities in binding energies per atom between the Al₄H₇⁻ cluster and the ones containing Be; this behavior can be explained by the proximity between Pauling electronegativities of Al (1.61) and Be (1.57). In addition, we evaluated two thermochemistry properties (the change in the enthalpies (ΔH) and the Gibbs free energy (ΔG)) as descriptors of the stability of these hydrides to be destroyed in individual atoms. The figures reported in the ESI† (Fig. SI-27) show the same result as the BE analysis: the systems doped with Be–H units exhibit the highest stability. Thinking in a future practical application, we found that the highest gravimetric hydrogen capacity (wt%) is obtained for systems substituted with Be–H units: 8.16, 11.1 and 15.6% for one, two and three Be–H replacements, respectively; while the substitutions with Mg–H units show a smaller increase: 7.75, 8.07, and 9.09%, for one, two and three Mg–H units, respectively. All values compared with the isoelectronic analogue Al₄H₇⁻ (6.09%). Since the Mg and Be hydrogen-rich doped systems are the ones closest to our system of interest (Al₄H₇⁻), we will

| Table 1 | Binding energy, per atom, for the systems doped with E–H units |
|---------|--------------------------------------------------|
|         | E₄Al₃H₈⁻ (eV) | E₄Al₂H₉⁻ (eV) | E₄AlH₁₀⁻ (eV) |
| Al      | 2.51           | 2.51           | 2.51           |
| Be      | 2.53           | 2.56           | 2.57           |
| Mg      | 2.41           | 2.33           | 2.22           |
| Ca      | 2.46           | 2.39           | 2.28           |
| Sr      | 2.44           | 2.36           | 2.23           |
| Ba      | 2.47           | 2.36           | 2.22           |

Fig. 5 Bonds recovery by the AdNDP analysis for Be₃Al₃H₈⁻, Be₂Al₂H₉⁻ and Be₃AlH₁₀⁻ systems. All occupations numbers (ON) are close to ideal value of 2.00 |e|.
continue our discussion analyzing the chemical bonding in them.

3.3 Multicenter chemical bonding analysis

The AdNDP results for Be–H and Mg–H replacements are presented in Fig. 5 and 6, respectively. A general observation is that in all the shown structures the hydrogen is incorporated forming metal–hydrogen 2c–2e bonds, where the hydrogen atoms are at the vertices of the structures, and forming metal–hydrogen–metal 3c–2e bonds, where the hydrogen atoms act as bridges, located at the edges. Another general observation is that Al₄H₇ → E₄Al₃H₈ → E₂Al₂H₉ → E₃AlH₁₀ transformations for E = Be and Mg, are characterized according to the changes in the nature and number of the multicenter σ-chemical bonds. An increase in the number of 3c–2e bonds of metal–hydrogen–metal type, Al–H–Al, Al–H–Be and Be–H–Be, as the substitutions by the Be–H units increase, is observed in Fig. 5: three, four and six bonds for the first, second and third Be–H replacement, respectively. Correlatively, a decrease in the number of intermetallic bonds (Al–Al and Al–Be–Al): two, one and cero bonds, for the first, second and third substitutions, respectively, is observed. A similar situation is presented with the substitutions by the Mg–H units (see Fig. 6): an increase in the number of metal–hydrogen–metal bonds (3c–2e): four, five and six bonds for the first, second and third Mg–H substitutions, respectively. Parallel to this, a decrease in the number of bonds associated to intermetallic interactions is observed: two, one and cero bonds, for the first, second and third Mg–H substitutions, respectively. For comparison, the AdNDP results for the Al₄H₇⁻ cluster are added in Fig. 6. Only two 3c–2e bonds of the Al–H–Al type, while three intermetallic bonds, two of Al–Al (2c–2e) type and one of the Al–Al–Al (3c–2e) type, are observed for this system.

The results above indicate that the excess of hydrogen, as the replacements increase, is incorporated in the metal–hydrogen–metal 3c–2e triangular units (being the metals of the same or of a different nature). These hydrogen atoms are in the form of hydrides, each of them stabilized simultaneously by two metals. Indeed, the increase of the metal–hydrogen–metal bonds, with the concomitant decrease of intermetallic bonds, as the Fig. 6 Bonds recovery by the AdNDP analysis for Al₄H₇⁻, MgAl₂H₈⁻, Mg₂Al₂H₉⁻ and Mg₃AlH₁₀⁻ systems. All occupations numbers (ON) are close to ideal value of 2.00 [e].

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replacements increase, occurs in a similar way for both, Be and Mg cases, though their relative energies between their structures are different. This indicates that the metal–hydrogen–metal units are fairly stable, and their three-center binding nature facilitates the weakening of intermetallic bindings. Therefore, as the aluminum atoms replacements increase, the bonding scheme tends to change from intermetallic bonds to bridge-like metal–hydrogen–metal bonds. This situation is evident in the case of the structures containing magnesium (Fig. 6).

Lastly, note that only beryllium atoms can form intermetallic bonds with aluminum atoms. As in the case of BEs, discussed in the previous section, this may be due to the closeness between Be and Al electronegativities. By contrast, Mg atom is less electronegative and cannot form covalent-like bonds.

### 3.4 Alkali complex

One of the main objectives of this work is to propose an alkali–clusters complex as a potential building block of cluster-assembled hydrides. For this purpose, we performed GEGA searches of the global minimum structures for the clusters containing Be and Mg. The resulting minimum energy structures are illustrated in Fig. 7 and 8.

For the beryllium clusters, the cage analogue of Al$_4$H$_7$– is stable only for one Be–H substitution, isomer located only to 0.6 kcal mol$^{-1}$ with respect to the global minimum (Iso-2). In the cases of two and three Be–H replacements, the tetrahedral analogues are located 4.2 and 9.2 kcal mol$^{-1}$, with respect to the global minimum, respectively.

The GEGA searches for the Mg-contained cases located the corresponding analogues of Al$_4$H$_7$– tetrahedral structure, with one and two Mg–H substitutions, at only +1.2 and +2.9 kcal mol$^{-1}$ from the global minima. However, this is not the case for three Mg–H substitutions, in which the tetrahedral-like cage is located at 8.6 kcal mol$^{-1}$ from the global minimum. Finally, two important results are reported in Fig. 7 and 8: (i) the global minima structures of NaBe$_2$Al$_2$H$_9$ and NaBe$_3$AlH$_{10}$ contains Be$_2$Al$_2$H$_9$– and Be$_3$AlH$_{10}$– hardly modified, and (ii) the global minimum obtained for NaMg$_3$AlH$_{10}$ has almost the same geometric shape of Mg$_3$AlH$_{10}$– (3E-1, at 0.0 in Fig. 1). Therefore, we can postulate these three alkali–cluster complexes as the potential building block to form cluster-assembled hydrides.
4. Conclusions

A strategy for the theoretical design of new atomic clusters with enhanced chemical and physical properties is presented in this work. The methodology consisted in systematically transforming, the stable Al₄H₇⁻ atomic cluster by successive isoelectronic substitutions of one aluminum atom by one E–H unity, where E = Be, Mg, Ca, Sr and Ba atoms. In a first stage, the searches on the potential energy surfaces (PES) for EAl₃H₈⁻, E₂Al₂H₉⁻, E₃AlH₁₀⁻ and E₄H₁₁⁻ systems, indicated that the tetrahedral-shape tends to be unfavored as the E–H units increase. Secondly, some electronic descriptors of stability as a Vertical Electron Affinity (VEA), Vertical Ionization Potential (VIP) and the HOMO–LUMO gap, suggest that systems composed by EAl₃H₈⁻, E₂Al₂H₉⁻, E₃AlH₁₀⁻ with E = Be and Mg atoms, should be the most stable atomic clusters. The capability of beryllium and magnesium atoms to form bridge 3c–2e (E–H–Al) plays a key role on the stabilization of these systems. Finally, the GEGA searches of alkali-complexes showed that NaBe₂Al₂H₁₀, NaBe₂AlH₁₀ and NaMg₂AlH₁₀ conformations have the same geometric shapes as the respective anionic systems, thus showing that these configurations are stable and can be postulated as potential building blocks to form cluster-assembled hydrides.

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