Identifying Ambiguous Similarity Conditions via Semantic Matching

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Abstract

Rich semantics inside an image result in its ambiguous relationship with others, i.e., two images could be similar in one condition but dissimilar in another. Given triplets like “aircraft” is similar to “bird” than “train”, Weakly Supervised Conditional Similarity Learning (WS-CSL) learns multiple embeddings to match semantic conditions without explicit condition labels such as “can fly”. However, similarity relationships in a triplet are uncertain except providing a condition. For example, the previous comparison becomes invalid once the conditional label changes to “is vehicle”. To this end, we introduce a novel evaluation criterion by predicting the comparison’s correctness after assigning the learned embeddings to their optimal conditions, which measures how much WS-CSL could cover latent semantics as the supervised model. Furthermore, we propose the Distance Induced Semantic Condition VERification Network (DISCOVER NET), which characterizes the instance-instance and triplets-condition relations in a “decompose-and-fuse” manner. To make the learned embeddings cover all semantics, DISCOVER NET utilizes a set module or an additional regularizer over the correspondence between a triplet and a condition. DISCOVER NET achieves state-of-the-art performance on benchmarks like UT-Zappos-50k and Celeb-A w.r.t. different criteria.

1. Introduction

Learning embeddings (a.k.a. representations) from data benefits machine learning and visual recognition systems [1, 6, 11, 25, 27, 39, 42, 43, 49]. Side information such as triplets [9, 10, 22, 29, 31] indicates the comparison relationship of objects, from which the embedding pulls visually similar objects close while pushing dissimilar ones away.

The linkage between objects conveys rich information about the object itself as well as its relationship with others, which becomes ambiguous when the similarity is measured from different perspectives. As illustrated in Fig. 1 (upper), (a) female with glasses, (b) female without glasses, and (c) male with glasses are organized in triplets.\footnote{In a valid triplet $(a, b, c)$, $(a, b)$ is more similar than $(a, c)$.} We think (a) and (b) are more similar when we measure based on “gender”. In contrast, we also treat (a) and (c) as neighbors since they “wear glasses”. Since one embedding space outputs fixed relationships between instances, learning multiple embeddings facilitates discovering rich semantics.

Given triplets associated with their condition labels, indicating under what kind of similarity the comparisons are made, Conditional Similarity Learning (CSL) learns multiple embeddings to cover latent semantic [36, 38]. During the evaluation, CSL predicts whether a triplet is meaningful or not under a specified condition. Although supervised CSL has been successfully applied in various applications [18, 19, 26, 34], labeling conditions introduces additional costs. As in a recommendation system, users may click relevant items (label item-wise similarities) based on particular preferences, and we only collect diverse comparison relationships without explicit condition labels [24, 32] propose Weakly Supervised-CSL (WS-CSL), where multiple embeddings are learned with triplets and the model is unaware of their corresponding conditions.

Figure 1. Upper: Two triplets with the same set of instances could be both meaningful when we measure similarity from different conditions. Lower Left: Given original (correct) triplets and their reversed variants (invalid w.r.t. the same similarity condition) on UT-Zappos-50k, we compute the proportion a model predicts them as valid ones. Last three are WS-CSL methods. Lower right: Our proposed criterion avoids the issue of reversed triplets naturally, and our DISCOVER NET outperforms other WS-CSL methods.
Current WS-CSL borrows the evaluation protocol from supervised CSL [36], which checks the validity of a triplet but neglects the specified condition. For example, we predict whether “aircraft” is similar to “bird” than “train” conditioned on “can fly” in the supervised scenario, but ask the model to predict the correctness of the triplet free from the condition in WS-CSL. Since a triplet could be ambiguous, WS-CSL may focus on weighting those embeddings to explain the triplet instead of learning semantically conditional embeddings corresponding to the ground-truth.

We demonstrate the challenge with the following experiment. After removing all condition labels of correct triplets, we compute the proportion a WS-CSL model predicts those triplets as valid ones via its learned embeddings, which equals the “accuracy” used in WS-CSL evaluation. Then we reverse those triplets — changing the order of the second and the third items, which makes them invalid under previous conditions. We further compute the valid ratio over reversed triplets. Results in Fig. 1 (lower left) show an optimal supervised model has 100% and 0% proportion/accuracy in two cases. A WS-CSL method SCE-Net [32] has a higher proportion than the supervised CSN [36] on original triplets as well as a high proportion on reversed ones, which means it treats both original and reversed triplets as valid. The diverse results between WS-CSL and its supervised counterparts indicate the “accuracy” is biased towards predicting all triplets as valid, and the correctness of a triplet without a specified condition is meaningless. To check the coverage of all semantics, we propose to measure the comparison ability of multiple learned embeddings after assigning them to target conditions.

We also propose Distance Induced Semantic Condition VERification Network (DISCOVERNET) to balance the ability of comparison prediction and semantic coverage. DISCOVERNET works in a “decompose-and-fuse” manner, which identifies similarity conditions and captures the ambiguous relationship with discriminative embeddings.

We aim to ensure the learned multiple embeddings in WS-CSL are able to reveal the similarities in the target conditions as much as the supervised methods. In DISCOVERNET, we achieve the goal from two aspects. First, we use a set module to map various triplets with the same set of instances to one condition, avoiding messy training update signals. On the other hand, we add a regularizer to force selecting different conditional embeddings when a model predicts both a triplet and its reversed one as valid. DISCOVERNET demonstrates higher performance on benchmarks like UT-Zappos-50k in our newly proposed criterion, which is shown in Fig. 1 (lower right). The code is available at https://github.com/shiyi19/DiscoverNet.

Our contributions could be summarized as:

• Based on the proposed DISCOVERNET, we improve the quality of learned embeddings and match the ground-truth semantics from two aspects.

• DISCOVERNET can identify latent rich conditions and works better than others in our criterion.

2. Related Work

Metric Learning. Learning embeddings from data attracts lots of attention in machine learning and computer vision. The learned embeddings encode the relationship between objects well and facilitate downstream tasks [4, 16, 27, 31]. With the guidance of the comparison relationship between object pairs [6], triplets [39, 43], and higher-order statistics [17], visually similar instances are pulled together, and visually dissimilar ones are pushed away. Types of loss functions are proposed [2,9,10,22,25,30,31] to take full advantage of the similarity comparisons between instances in a mini-batch, e.g., the triplet loss [27] and N-Pair loss [29].

Conditional Similarity Learning (CSL). Different from measuring all linkages with a single metric, the relationship between objects could be measured from diverse aspects (under different conditions) [3,23,33]. In [36,46], CSL is investigated by associating conditions with image attributes, and multiple diverse embeddings could be derived from feature masks to capture the semantic of various conditions. CSL has been applied in applications like image-text classification [20,24], fashion retrieval [8,15,32], zero-shot learning [48] and video grounding [28]. Condition labels during training link a particular embedding with a condition, and the learned embeddings are evaluated by predicting the validity of a triplet under a certain condition.

Weakly supervised CSL. Noticing condition labels are unavailable in some cases, e.g., we get a comparison tuple once a user selects an item than others without any knowledge of his/her preference (condition). The weakly supervised CSL, i.e., learning conditional embeddings without condition annotations is investigated in [1], where a model infers conditions given a triplet and then decides the right embedding to use for training and deployment. [32] emphasizes the comparison ability of the fused embedding, while [24,42] select one metric from multiple candidates to explain a triplet. Using the same evaluation protocols as CSL, weakly supervised CSL can get higher performance than supervised CSL without involving the ground-truth condition labels. We analyze the protocol and point out its drawbacks of semantic coverage. We propose a new criterion to reveal the difference between the quality of the learned embedding and its supervised counterpart. We also propose DISCOVERNET to trade-off the diversified embedding and semantic fusion in a “decompose and fuse” manner. A set module and a semantic regularizer are discussed to make DISCOVERNET cover all target conditions.
3. Notations and Background

We organize comparisons into triplets, i.e., $\mathcal{T} = \{\tau = (x, y, z)\}$. For three items in $\tau$: the anchor $x \in \mathbb{R}^D$ has a similar target neighbor $y \in \mathbb{R}^D$, and an impostor $z \in \mathbb{R}^D$ is dissimilar with $x$. Similarity in $\tau$ could be determined by categories of instances. The embedding, a.k.a., feature extractor, $\phi : \mathbb{R}^D \rightarrow \mathbb{R}^{d'}$ projects an instance $x$ into a latent space, whose distance with $y$ is

$$\text{Dis}_L^2(\phi(x), \phi(y)) = \|L^\top(\phi(x) - \phi(y))\|^2_2. \quad (1)$$

$L \in \mathbb{R}^{d \times d'}$ is a projection. We implement $\phi$ with deep neural network, and learn embedding by minimizing the violation of comparisons over $|\mathcal{T}|$ triplets. Define the validness of a triplet $\tau$ by comparing the distances between “anchor-impostor” and “anchor-target neighbor”, i.e.,

$$\text{Diff}_\tau = \text{Dis}_L^2(\phi(x), \phi(z)) - \text{Dis}_L^2(\phi(x), \phi(y)). \quad (2)$$

If the anchor has a larger distance with the impostor than with the target neighbor, the embedding is consistent with the relationship in $\tau$. Given a loss $\ell(\cdot)$, e.g., the margin loss or the logistic loss, we optimize $\min_{\phi, L} \sum_{\tau \in \mathcal{T}} \ell(\text{Diff}_\tau - \gamma)$. Then $\text{Diff}_\tau$ would be larger than the margin $\gamma$, so that anchor and the target neighbor are pulled while the impostor would be pushed away.

**Conditional similarity learning (CSL).** Comparisons in triplet $\tau$ may vary across environments. For example, when we ask which image in a candidate set is close to a given anchor, different workers may measure the similarities from their own aspects. In CSL, we associate a condition label $k \in \{1, \ldots, K\}$ with each triplet, i.e., $\mathcal{T} = \{\tau = (x, y, z, k)\}$, indicating based on the $k$-th condition the comparison in $\tau$ is made. One embedding $\phi$ fails to capture the diverse relationship when comparisons with the same set of instances are opposite, e.g., $\tau_1 = (x, y, z, k)$ vs. $\tau_2 = (x, z, y, k')$. CSL extends $\phi$, $L$, and $\text{Diff}_\tau$ to $\phi_k$, $L_k$, and $\text{Diff}_\tau^k$, respectively. $K$ embeddings $\Psi_K$ covering $K$ conditions are optimized:

$$\min_{\Psi_K = \{\psi_k = L_k \circ \phi_k\}_{k=1}^{K}} \sum_{\tau \in \mathcal{T}} \Bigg( \sum_{k'=1}^{K} I[k' = k] \left[ \text{Diff}_{\tau}^{k'} - \gamma \right] \Bigg). \quad (3)$$

$I[\cdot]$ outputs 1 when the input is true and 0 otherwise. In Eq. 3, only the distance corresponding to condition $k$ of the triplet $\tau$ is activated. In evaluation, $\psi_k$ is used to check whether a triplet from the $k$-th condition is valid or not.

**Weakly supervised CSL (WS-CSL).** Due to additional annotation costs and ambiguity of condition labels, the triplet-wise condition labels $\{k\}$ are unknown in WS-CSL. The model needs to infer condition labels and activates the corresponding embeddings to capture triplet’s characteristic. The target of WS-CSL is to learn a set of embeddings $\Psi_K$, which is able to capture those semantics of target conditions as much as the supervised CSL.

4. Evaluation of Weakly Supervised CSL

Current WS-CSL follows CSL to measure $\psi_k$ by predicting whether three instances could form a triplet without a condition label. We analyze the issues of the current criterion and propose our new evaluation protocol.

4.1. Analysis of Supervised CSL Evaluation

In supervised CSL evaluation, a model is asked to determine whether a triplet $\tau_1 = (x, y, z, k)$ is valid or not given the condition $k$. In detail, we get $\text{Diff}_\tau^k$ with the corresponding conditional embedding $\psi_k$ and predict $\tau_1$ as valid if $\text{Diff}_\tau^k > 0$. Since $\tau_1 = (x, y, z, k)$ and $\tau_2 = (x, z, y, k')$ could not co-exist, we sample the same number of valid triplets from each condition in evaluation. The average accuracy (proportion of triplets predicted as correct) over them reveals the quality of a CSL model.

Since the ability of comparison prediction is important, previous WS-CSL methods follow this protocol without using the test-time condition labels. In other words, we predict whether a triplet $\tau_3 = (x, y, z)$ is correct without its condition label. So in this case, a WS-CSL model predicts the validness of a triplet with all learned embeddings.

There are two issues when evaluating with the supervised protocol directly. First, a model tends to find a condition
to explain the triplet, which predicts all triplets as true in most cases, e.g., even for reversed triplets (demonstrated in Fig. 1). Specifically, given a valid \( \tau_1 = (x, y, z, k) \), we construct \( \tau_2 = (x, z, y, k) \), and ask a WS-CSL model whether \( \tau_3 = (x, z, y) \) is valid or not. Since \( \tau_2 \) is invalid under the same condition \( k \), an optimal supervised model will predict \( \tau_1 \) as true and \( \tau_2 \) as false. However, a WS-CSL method SCE-Net [32] predicts most original (\( \tau_3 \)) and reversed (\( \tau_4 \)) triplets as valid, which makes the evaluation biased.

Moreover, the current evaluation predicts the validity of the triplet while neglecting from which condition the WS-CSL model determines the relationship. We’d like a WS-CSL model works similarly to a supervised one, so not only the fusion of conditional embeddings \( \Psi_k \) should cover all target semantics, but also the behavior of each \( \psi_k \) reveals the relationship w.r.t. a specific condition. Therefore, we propose a new criterion to meet the previous requirements.

4.2. Condition Alignment for WS-CSL Evaluation

We claim that predicting the validity of a triplet is only meaningful given a specific condition. Based on the ground-truth conditions and the validity of triplets during the evaluation, we propose a two-step new criterion. First, we map target conditions to WS-CSL embeddings \( \Psi_K \). Then, we evaluate triplets accuracy with corresponding \( \psi_k \) as in the supervised scenario, which reveals how much a WS-CSL model covers the target conditions as the supervised model.

We assume there is the same number of embeddings and conditions.\(^2\) Given triplets from the \( k \)-th condition for evaluation, we compute the triplet prediction accuracy with \( \{\psi_{k'}\}_{k'=1}^K \). We collect accuracy for all conditions and form a cost matrix \( C \in \mathbb{R}^{K \times K} \), whose element \( C_{k'k} \) is the error (100 minus the accuracy) using \( k' \)-th embedding to predict the triplets from the \( k \)-th condition. The alignment could be obtained from \( C \) with the following two strategies.

Greedy Alignment. We use a greedy strategy to find the most suitable embedding, i.e., \( \arg \min \psi_k \in \{\psi_{k'}\} \) for a condition \( k \). So one embedding may handle multiple conditions.

OT Alignment. We optimize the following Optimal Transport (OT) objective [37] to obtain a mapping \( T \in \mathbb{R}^{K \times K} \) from the embedding set to the condition set

\[
\min_{T \succeq 0} \langle T, C \rangle \quad \text{s.t.} \quad T \mathbf{1} = \frac{1}{K} \mathbf{1}, \quad T^\top \mathbf{1} = \frac{1}{K} \mathbf{1}. \tag{4}
\]

Eq. 4 minimizes the total cost when we use an embedding to predict triplets from another condition. We set the marginal distribution of the transportation \( T \) as uniform. By minimizing Eq. 4 we obtain \( T \) as a map. Element \( T_{k'k} \) reveals how much the \( k' \)-th embedding is related to the \( k \)-th condition. We can further obtain a one-to-one mapping based on \( T \) under assumptions [5]. Fig. 2 shows a comparison between our proposed and previous criteria.

\(^2\)Our analysis could be extended when their numbers do not match.
5.1. Decompose and Fuse Hierarchical Spaces

We assume condition-specific embeddings $\Psi$ have different projections $L_k$ but share the same $\phi$. Then we have

$$\text{Diff}^k_\tau = \text{Dis}^2_{L_k} (\phi(x), \phi(z)) - \text{Dis}^2_{L_k} (\phi(x), \phi(y)) \quad (5)$$

The space measured by projection $L_k$ biases towards a “local” view of the embedding $\phi$, and allows inconsistent comparisons across different “instance-instance” spaces.

The overall linkages between objects are measured based on a fused distance over condition-specific comparisons. Different from the indicator in Eq. 3 selecting the distance, we use a multinomial distributed variable $c_\tau \in \{0, 1\}^K$ to denote the latent condition label of a triplet $\tau$. There are $K$ binary elements in $c_\tau$. We optimize $\phi$ and $L_K$ jointly:

$$\min_{\phi, L_K} \sum_{\tau \in T} \ell \left( E_{c_\tau} \left[ \text{Diff}^k_\tau - \gamma \right] \right). \quad (6)$$

The condition of the triplet is revealed by the expected distance w.r.t. the distribution of $c_\tau$, [44], which selects or fuses the related conditions of the triplet. If a triplet could only be valid under the $k$-th condition, we expect $c_\tau$ has the $k$-th element $c_\tau^k = 1$ and other elements equal 0. Then the expected distance activates the $k$-th metric, and the target neighbor (resp. impostor) is pulled close (resp. pushed away) with $L_k$. The $k$-th embedding becomes more specific for the condition. If the triplet is related to more conditions, we expect $\tau$ to fuse the semantics from multiple distances together. Therefore, values in $\tau$ determine whether to select or fuse conditional embeddings, which emphasizes the semantic coverage or comparison prediction, respectively.

Given $E_{c_\tau} \left[ \text{Diff}^k_\tau \right] = \sum_{k=1}^{K} \text{Pr}(c_\tau^k = 1) \text{Diff}^k_\tau$, the variable $c_\tau$ indicates the influence of the posterior probability $\text{Pr}(c_\tau^k = 1)$ that a triplet belongs to the $k$-th condition. We introduce a “triplets-condition” space, where a triplet is embedded to a point with mapping $g(\cdot)$. $g$ summarizes the triplet $\tau$ and maps the set of embeddings in $\tau$ into a $d$-dimensional vector. We expect triplets with similar conditions will be close. Furthermore, $K$ learnable anchors $\{a_k \in \mathbb{R}^d\}_{k=1}^K$ captures those similarity conditions, and we match a triplet to its closest anchor:

$$\text{Pr}(c_\tau^k = 1) \sim \text{Sim}(g(\tau), a_k)$$

$$= \frac{\exp \left( \cos(g(\tau), a_k) / \varsigma \right)}{\sum_k \exp \left( \cos(g(\tau), a_k) / \varsigma \right)}. \quad (7)$$

We implement the similarity with cosine. $\varsigma > 0$ is the temperature. The larger the $\varsigma$, the more uniform $\text{Pr}(c_\tau^k = 1)$ is. If a triplet is related to the $k$-th condition, then its transformed vector $g(\tau)$ is close to the anchor $a_k$. Then a larger

3Since conditions are not independent, it is not necessary to match each condition with an embedding $\psi_k$. More discussions are in experiments.

Figure 4. Illustration of the set module (left) and semantic regularization (right) to deal with artificially reversed triplets.

$\text{Sim}(g(\tau), a_k)$ emphasizes the $k$-th condition when computing the expected distance. Benefited from the “decompose and fuse” manner in Eq. 7, a triplet that has a clear condition tendency will be close to a particular anchor, which makes $c_\tau$ becomes one-hot, and the embedding is highly correlated with the corresponding condition. Then embeddings will cover more semantics. Those ambiguous triplets will have a nearly uniform $c_\tau$. Although hard to differentiate semantics in this case, their fused distances take advantage of all embeddings to predict the validness of triplets and improve the comparison prediction ability.

Instance Space for Semantic Discovery. Given $L_k \in \mathbb{R}^{d \times d}$, we define the $k$-th conditional embedding $\psi_k(x)$ as

$$\psi_k(x) = \phi(x)(I + L_k) = \phi(x) + \phi(x)L_k. \quad (8)$$

We obtain the local embedding $\psi_k(x)$ in a residual form, where $L_k$ encodes the similarity bias of the $k$-th condition based on the general embedding $\phi$. If $\phi$ is discriminative enough for a particular similarity condition, we do not need to over-allocate the local metric. In other words, strong $\phi$ makes $L_k$ degenerate to zero. In summary, distances for different similarity conditions in Eq. 5 are calculated based on $\psi_k$.

5.2. Condition Space for Semantic Fusion

Based on our analyses in Section 4, a WS-CSL model could violate the semantic constraints in vanilla training. A too flexible mapping $g$ will make the model treat both a triplet and its reversed version as correct ones while activating almost the same conditional embedding $\psi_k$. In other words, the model may focus on fusing those conditions with $g$ and collapse all semantics into one conditional space.

Since semantic constraints on a WS-CSL model are limited, we address the issue with the help of artificially reversed triplets. For a pair of original triplet and its reversed version, we restrict the model’s flexibility by either weakening the representation ability of $g$ with a set module or adding another semantic regularizer (illustrated in Fig. 4).
Set Module. A natural way to implement $g$ is to capture the order of instances in a triplet with a sequential model [14, 32]. As we mentioned, a triplet $τ_1 = (x,y,z)$ and its reversed version $τ_2 = (x,z,y)$ should belong to different conditions. However, without any constraints, we find a sequential module has the ability to weight conditions in different manners for $τ_1$ and $τ_2$, but it is likely to work in a “lazy” way. In detail, a model may learn a strong conditional embedding associated with corresponding conditional semantic meanings, a model tends to improve the fusion module and use partial embeddings to cover all semantics.

Therefore, we consider a set module to make $g$ agnostic with the order in the triplet. In particular, we use the pairwise concatenation of instance embeddings as the input of $g$, i.e., for a triplet $τ_1$, we obtain its embeddings, $φ(τ) = (φ(x), φ(y), φ(z))$ and get the augmented set: $P = \{[φ(x), φ(y)], [φ(x), φ(z)]\}$, which encodes the pairs in $τ_1$. Since $[φ(y), φ(z)]$ is not included in $P$, we get the same representation for $τ_1$ and the reversed $τ_2$. Moreover, to take a holistic view of $τ$, we transform with element-wise maximization [47]:

$$g(τ) = FC \max_{p \in P} FC(p). \tag{9}$$

$FC$ is a fully connected network with one hidden layer and ReLU activation, which projects the given input to a same-dimensional output. With Eq. 9, the pairwise relationship in the triplet is evaluated first, and the most evident one is activated to represent the whole triplet. In summary, the set module restricts the ability of $g$ and makes one triplet and its reversed version have the same representation. Although it is a bit counter-intuitive, the special configuration of $g$ avoids the ambiguous update directions of the model so that the conditional embeddings should be more discriminative to cover the target semantics. We also investigate the Transformer [35] implementation of $g$ in the supplementary. **Semantic Regularizer.** We can also think from another aspect by regularizing a representative $g$. We set Eq. 9 to

$$P = \{[φ(x), φ(y)], [φ(x), φ(z)], [φ(y), φ(z)]\},$$

covering the sequential information of instances. Due to an additional pair in $P$, different orders of instances in $τ_1$ and $τ_2$ do not share the same output. In this case, it is abnormal when the model predicts $τ_1$ and $τ_2$ based on the same condition $k$. We construct a semantic regularization to avoid this case. If $\text{Diff}^k_{τ_1} > 0$ and $\text{Diff}^k_{τ_2} > 0$ (the model treats two triplets as valid ones), we add the following semantic regularizer to make the activated conditions diverse:

$$\text{Reg}(g) = λ \sum_{k=1}^K \min \left(\text{Sim}(g(τ_1), a_k), \text{Sim}(g(τ_2), a_k)\right). \tag{10}$$

In other words, if $τ_1$ and $τ_2$ are predicted as valid ones, we minimize the similarity between their condition distributions $c_{τ_1}$ and $c_{τ_2}$. The similarity between these two multinomial distributions is measured with Histogram Intersection Kernel (HIK) [12, 40, 41], which is the sum of element-wise minimum of two distributions. Therefore, with the help of Eq. 10, we explicitly enforce the WS-CSL model considers different conditional embeddings to explain triplets, which further improve the semantic coverage of $Ψ_K$.

**Discussions.** There are two implementations of DISCOVERNET, using the set module or the semantic regularizer. The two strategies are designed from different aspects to make the WS-CSL model contain rich semantics as much as the supervised model. Since the set module avoids the diverse selection for reversed triplet naturally, it satisfies the regularizer directly. Thus, it does not help if we combine two strategies together.

6. Experiments

We verify the effectiveness of DISCOVERNET over benchmarks based on our new criterion. Ablation studies and visualization results demonstrate DISCOVERNET learns conditions successfully as the supervised methods. Detailed setups and more results are in the supplementary.

6.1. Experimental Setups

Datasets. UT-Zappos-50k Shoes contains 50,025 images of shoes with four similarity conditions collected online [45, 46]. Following [24, 32, 36], we discretize the “height” condition and resize all images to 112 by 112. There are 200,000, 20,000, and 40,000 triplets following splits in [36] for training, validation and test, respectively. Celeb-A Faces has 202,599 face images of different identities [21]. 8 of the 40 attributes (conditions) are selected for analysis [24]. We resize all images to 112 by 112. 400,000/80,000/160,000 triplets are used for model training/validation/test. We construct a more difficult Celeb-A by combining related binary attributes in Celeb-A together, where each multi-choice condition has 5-7 discrete values. We apply the same configuration for Celeb-A variants.

Splits. All models are trained and evaluated over triplets in [36]. Since there are no published triplets over Celeb-A, we randomly sample triplets by ourselves. Equal number of triplets for each attribute are sampled from the standard training, validation, and test split of Celeb-A [21]. For each triplet, we organize instances with the same attribute label into a similar pair. Otherwise, we think they are dissimilar.

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Footnote:

4We check this condition with the current model during training. Parameters in $\text{Diff}^k$ are detached without gradient back propagation.
Table 1. GR accuracy and OT accuracy on UT-Zappos-50k. We investigate two cases that training the model from scratch and fine-tune the model with pre-trained weights. CSN is the fully supervised CSL method which utilizes condition labels during training. We make the best WS-CSL results in each case in bold.

| Setups | Criteria | w/ pretrain | w/o pretrain |
|--------|----------|-------------|--------------|
| CSN [36] | GR Acc. | 87.86 | 82.14 |
| | OT Acc. | 87.86 | 82.14 |
| LSN [24] | GR Acc. | 76.26 | 71.49 |
| | OT Acc. | 75.90 | 68.49 |
| SCE-Net [32] | GR Acc. | 72.21 | 64.08 |
| | OT Acc. | 71.15 | 61.03 |
| DISCOVERNET_{Set} | GR Acc. | 76.98 | 74.67 |
| | OT Acc. | 75.68 | 74.13 |
| DISCOVERNET_{Reg} | GR Acc. | 77.84 | 72.99 |
| | OT Acc. | 77.68 | 71.46 |

**Criterion.** We utilize our proposed new criterion to evaluate WS-CSL methods. After constructing a mapping from condition to learned embeddings with greedy or OT strategies, we compute the average triplet prediction accuracy as in the supervised case. We denote the results with two strategies as GR Accuracy and OT Accuracy, respectively.

**Comparison Methods.** We compare DISCOVERNET with both supervised method Conditional Similarity Networks (CSN) [36] and two WS-CSL methods, i.e., Latent Similarity Networks (LSN) [24] and Similarity Condition Embedding Network (SCE-Net) [32].

**Implementation Details.** Following [24, 32, 36], we use ResNet-18 [13] to implement $\phi$. Different from previous literature fine-tuning the backbone based on the weights pre-trained on ImageNet [7], we also consider the case that we train the full model from scratch. The model with the best accuracy over the validation set is selected for the final test.

### 6.2. Benchmark Evaluations

**UT-Zappos-50k.** The results of DISCOVERNET and comparison methods over UT-Zappos-50k are listed in Table 1, which contains the greedy accuracy and OT accuracy over both pre-trained and non-pre-trained weights. We re-implement all comparison methods. DISCOVERNET_{Set} and DISCOVERNET_{Reg} denote the variant using set module and semantic regularization, respectively.

By observing both setups and criteria, CSN becomes the “upper-bound” for WS-CSL methods. The main reason is that ground-truth condition labels in CSN associate an embedding with a particular condition during training. The supervised CSN gets the same greedy and OT accuracy. The explicit supervision in CSN makes those embeddings biased towards different semantics, which gets the same one-to-one OT mapping with the greedy strategy. WS-CSL methods get lower OT accuracy than the corresponding greedy accuracy. The main reason is that OT accuracy requires a one-to-one mapping between embeddings and conditions, where those conditions would be related. While greedy accuracy allows one embedding to handle multiple conditions.

As we discussed before, SCE-Net tends to fuse the semantic meaning of embeddings with its self-attention module, so each of its learned embeddings is hard to cover a specific condition. By contrast, LSN performs better in our criteria, benefiting from its multi-choice learning paradigm. Our DISCOVERNET can get the best performance among WS-CSL methods. In detail, DISCOVERNET_{Set} works better when training from scratch and DISCOVERNET_{Reg} performs well with the pre-trained weights. One possible reason is that the pre-trained weights are strong and make the model (especially the mapping function $g$) too flexible, so an explicit regularization helps more. In summary, our criterion reveals how much similar a WS-CSL model performs to a supervised one.

**Celeb-A.** In Table 2, we investigate (the 8 attribute) Celeb-A and its variant Celeb-A † with five multi-choice conditions, respectively. All methods are trained from scratch. More results are in the supplementary.

**Criteria**

| Celeb-A | Celeb-A † |
|---------|-----------|
| CSN [36] | 83.41 | 67.72 |
| LSN [24] | 79.29 | 57.02 |
| SCE-Net [32] | 69.47 | 51.49 |

**Comparisons**

| DISCOVERNET_{Set} | DISCOVERNET_{Reg} |
|--------------------|--------------------|
| GR Acc. | OT Acc. | GR Acc. | OT Acc. |
| 78.45 | 77.98 | 64.57 | 63.98 |

**Table 2. Greedy accuracy and OT accuracy on 8-condition Celeb-A (binary conditions) and its attribute merged variant Celeb-A † with five multi-choice conditions, respectively. All methods are trained from scratch. More results are in the supplementary.**

**Table 3. Influence of the embedding number (the number of projections in $L_K$) for DISCOVERNET_{Set} and DISCOVERNET_{Reg} on Celeb-A. Models are fine-tuned with pre-trained weights.**

| # Projections | DISCOVERNET_{Set} | DISCOVERNET_{Reg} |
|---------------|--------------------|--------------------|
| GR Acc. | OT Acc. | GR Acc. | OT Acc. |
| 2 | 78.28 | 77.74 | 71.92 | 71.82 |
| 4 | 79.58 | 77.60 | 73.19 | 71.32 |
| 6 | 80.41 | 77.69 | 75.53 | 73.87 |
| 8 | 80.65 | 78.81 | 75.19 | 74.07 |
| 10 | 81.35 | 78.68 | 76.09 | 73.77 |
Figure 5. TSNE of the learned embeddings for each of the four conditions (i.e., functional types, closing mechanism, suggested gender and height of heels) on UT-Zappos-50k dataset based on DiscoverNetReg.

Figure 6. Visualization of the image retrieval results for each of the four conditions on Celeb-A with the learned embedding of DiscoverNetReg. The first image in each row is the anchor, and faces are ranked by distances to the anchor in an ascending order.

Visualization of semantic embeddings. To better illustrate how our DiscoverNet learns for different semantics, we provide TSNE visualizations for each of the learned semantic spaces \( \psi_k \) on UT-Zappos-50k in Fig. 5. DiscoverNet captures the variety of conditions and learns different embeddings for the dataset with good interpretability. Typically, on the condition “height of heels”, the heel height of the shoes is decreasing from the left-top of the embedding space to the bottom, then to the right-top.

Visualization of conditional image retrieval. We provide image-retrieval visualizations for four conditions on Celeb-A in Fig. 6. We keep the anchor image, and retrieve its neighbor from a set of randomly collected candidates with different local embeddings. Benefiting from the correspondence obtained when computing the OT accuracy, we can qualitatively measure whether a local embedding could reveal the corresponding semantic via its ranking of images. For example, on the “Male” condition, since the anchor image has the label “Female”, DiscoverNet makes all images labeled “Female” close while pushing images related to “Male” away. The results indicate our DiscoverNet can cover latent semantics of data and each of its learned conditional embedding \( \psi_k \) corresponds to a particular meaningful semantic.

7. Conclusion

We revisit WS-CSL and observe that evaluating the quality of the model without specifying concrete conditions produces biased accuracy. Thus, we match multiple learned embeddings with ground-truth conditions in advance before predicting the correctness of given triplets, which simultaneously considers the ability of triplet prediction and semantic coverage. We also utilize a set module or a semantic regularizer in our proposed DiscoverNet to emphasize the correspondence between a conditional embedding and a semantic condition. DiscoverNet outperforms other WS-CSL methods on benchmarks with different criteria.

Limitations. Our new criterion evaluates WS-CSL in a “supervised” manner by assigning multiple learned embeddings to target conditions. The criterion does not fit the case when the goal is not to learn a model similar to its supervised counterpart, e.g., to distinguish whether triplets are correct and explain their validness as much as possible.

Acknowledgments. This research was supported by National Key R&D Program of China (2020AAA0109401), NSFC (62006112, 61921006, 62176117), Collaborative Innovation Center of Novel Software Technology and Industrialization, NSF of Jiangsu Province (BK20200313).
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