The Influence of Bi$_2$O$_3$ Nanoparticle Content on the γ-ray Interaction Parameters of Silicon Rubber

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Abstract: In this study, synthetic silicone rubber (SR) and Bi$_2$O$_3$ micro- and nanoparticles were purchased. The percentages for both sizes of Bi$_2$O$_3$ were 10, 20 and 30 wt% as fillers. The morphological, mechanical and shielding properties were determined for all the prepared samples. The Linear Attenuation Coefficient (LAC) values of the silicon rubber (SR) without Bi$_2$O$_3$ and with 5, 10, 30 and 30% Bi$_2$O$_3$ (in micro and nano sizes) were experimentally measured using different radioactive point sources in the energy range varying from 0.06 to 1.333 MeV. Additionally, we theoretically calculated the LAC for SR with micro-Bi$_2$O$_3$ using XCOM software. A good agreement was noticed between the two methods. The NaI (TI) scintillation detector and four radioactive point sources (Am-241, Ba-133, Cs-137 and Co-60) were used in the measurements. Other shielding parameters were calculated for the prepared samples, such as the Half Value Layer (HVL), Mean Free Path (MFP) and Radiation Protection Efficiency (RPE), all of which proved that adding nano-Bi$_2$O$_3$ ratios of SR produces higher shielding efficiency than its micro counterpart.

Keywords: silicon rubber; nano-Bi$_2$O$_3$; LAC; RPE; HVL

1. Introduction

In medical facilities, such as hospitals, clinics, outpatient care centers, radiological centers and dental facilities, where ionizing radiation is widely utilized, planning is compulsory to protect patients and medical staff who are usually exposed to different types of radiation. For this reason, it is important to use radiation protection materials, whether or not these materials are worn, such as eyeglasses, neck guards or an apron [1–4]. Moreover, it is important to utilize specific materials to insulate the walls of the medical facilities in order to prevent radiation leakage into the surrounding environment. This applies not only to the medical facilities, but also all facilities that utilize gamma radiation or X-ray, such as universities and research laboratories, nuclear power plants, and factories [5,6].

The attenuation properties for the radiation protection medium must be accurately known when planning to design any facility that uses gamma rays and X-rays, so that appropriate protection is provided for patients, workers, visitors, and the surrounding environment [7–9]. The radiation protection properties of a medium depend on its density as well as the chemical composition of the medium’s constituent materials. Thickness is also considered as another factor that affects the shielding properties of a given medium. The traditional materials that are practically used in radiation protection applications have several drawbacks.

Some of these materials are expensive and some are heavy, and this limits their use in practical applications. For example, tungsten has a higher number of attenuation factors...
than lead; it also has a high cost and this prevents tungsten from being widely used in real applications. Recently, researchers turned to the production of radiation protective clothing that is characterized by its low cost, light weight, easy use, comfort and, most importantly, its protection of workers in the field of ionizing radiation [10–12]. In this regard, some additives are usually added to the flexible materials to fabricate protective garments, such as aprons or curtains. In practical applications, vinyl, polymers and rubbers are one of the most widespread materials used as matrix materials to obtain flexible protection materials, while bismuth, tungsten and antimony powders are used as additives. The importance of such additives is to increase the possibilities of the photon interactions with the atoms of the prepared flexible protective materials.

As is known, the polymers and plastics have a relatively low density and this, to a certain degree, produces their ability to attenuate photons. Therefore, these plastic materials are usually used to attenuate low-energy radiation [13–15]. In order to increase its density and thus improve its shielding performance, especially if it is exposed to photons of medium energy, bismuth is used [16,17]. Silicone rubber (SR) is an important matrix material that has good elasticity features. In the past few years, some researchers used silicone rubber to develop flexible radiation shielding materials. Kameesy et al. [18] fabricated SR sheets filled with four concentrations of PbO. They experimentally evaluated the radiation attenuation factors for the prepared SR-PbO campsites using different radioactive sources. They found that adding PbO to the SR enhances the physico-mechanical features. Gong et al. [19] fabricated a novel radiation protection composite based on methyl vinyl silicone rubber. The authors found that when benzophenone is added to the matrix, a notable enhancement in the radiation resistance occurs. Based on their results, the transmission of the photon with energy of 0.662 MeV through a sample thickness of 2 cm is only 0.7. Özdemir and Yılmaz [20] prepared a mixed radiation shielding via 3-layered polydimethylsiloxane rubber composite. The three layers were composed of hexagonal boron nitride, B₂O₃ and Bi₂O₃. They developed a shielding material that possesses a lead equivalent thickness of 0.35 mm Pb. Chai et al. [21] prepared new flexible shielding material using methyl vinyl silicone rubber. They used zinc borate, B₄C and hollow beads as filler materials. They evaluated the neutron shielding performance of their flexible material of the thermal neutron transmission technique with the help of an Am–Be radiation source. However, even though different research groups studied the SR as flexible shielding materials, there is still an urgent need for the further development of novel flexible materials using Bi₂O₃ as a filler in nano and micro sizes. Therefore, in this study, we develop a new flexible material against X-ray and γ-ray photons based on Bi₂O₃ nanoparticle content.

2. Materials and Methods

2.1. Matrix

Vulcanized silicone rubber was used as a flexible matrix material. The most common form of silicone is the polydimethylsiloxane polymer, which is liquid in origin. This polymer is a rigid structure of elastomers transformed by catalyzed cross-linking reactions [22]. To obtain catalyzed cross-linking reactions, a stiffener with 4% (by weight) must be added to the silicon rubber. The specific gravity of SR was 1.12 g/mL and the elongation was 350%. The main elements of SR are hydrogen, carbon, oxygen and silicon, as shown in Figure 1.

![Figure 1. The structure of silicon rubber.](image_url)
2.2. Fillers

Bismuth oxide (Bi$_2$O$_3$) of micro and nano sizes was used as a filler in the composite. Before adding it to the solution, a transmission electron microscope (TEM) is used to image the powder to ensure the size of the particles, as shown in Figure 2. The average size of the microparticles was 15 ± 5 µm, while the average size of the nanoparticles was 30 ± 5 nm.

![Figure 2. TEM images for (a) Bi$_2$O$_3$ microparticles and (b) Bi$_2$O$_3$ nanoparticles.](image)

2.3. Composites

Seven different SR samples were prepared. Codes, compositions and densities of the prepared samples are tabulated in Table 1. The homogenous mixtures (liquid SR + micro or nanoparticles of Bi$_2$O$_3$ + stiffener) were poured into cylinder molds, which had a 3 cm diameter and different thicknesses (0.3, 0.66, 0.93 and 1.3 cm). The prepared samples waited for 24 h to become elastic-solid materials. The density of the SR sample is measured via the mass/volume, the volume of the sample is calculated by ($\pi r^2 \cdot x$), where $r$ is the radius and $x$ is the thickness of the measured sample.

| Code    | Compositions (wt%)       | Density (g/cm$^3$) |
|---------|--------------------------|--------------------|
| SR-0    | 100 - -                  | 1.191              |
| SR-5m   | 95 5 -                   | 1.301              |
| SR-5n   | 95 - 5                   | 1.351              |
| SR-10m  | 90 10 -                  | 1.368              |
| SR-20m  | 80 20 -                  | 1.509              |
| SR-30m  | 70 30 -                  | 1.684              |
| SR-30n  | 70 - 30                 | 1.713              |

2.4. Morphological Images

A scanning electron microscope (SEM) of JSM-5300, JEOL model, Tokyo, Japan was used for scanning the images of the prepared SR samples. The samples were coated using an ion sputtering coating device (JEOL-JFC-1100E, Tokyo, Japan), and then the samples were placed inside the electron microscope with an operating voltage of 20 keV [23].

2.5. Mechanical Properties

The tensile strength, Young’s modulus and elongation at break were determined for the present SR samples using an electronic tensile testing machine (model 1425, Germany), according to standard methods with ASTM D412. The Shore hardness was measured according to ASTM D2240.
2.6. Shielding Properties

The linear attenuation coefficient (LAC) was measured for all discussed SR samples using the narrow beam technique of gamma ray spectroscopy in a radiation physics laboratory (Faculty of Science, Alexandria University, Alexandria, Egypt). The devices used in this method were the detector, collimator and radioactive point sources. An NaI (TI) cylindrical scintillation detector with a (3” × 3”) dimension, a relative efficiency of 15% and an energy value of Cs-137 (0.662 MeV) was used. The inner diameter of the lead collimator was 8 mm and the outer diameter was 100 mm. The point radioactive sources were chosen to cover a wide range of energy, where four radioactive sources were used as follows: Am-241 (0.06 MeV), Ba-133 (0.081, 0.356 MeV), Cs-137 (0.662 MeV) and Co-60 (1.173, 1.333 MeV) [24–29]. The illustration of the experimental setup is shown in Figure 3.

The intensity (I₀), count rate (N₀) or area under the peak (A₀) were measured for all energies in a case without the SR sample, and then the sample was placed between the source and detector and the count rate (N) or area under the peak (A) was measured at the same time. The LAC was measured experimentally using the following equation [30,31]:

\[
LAC = \frac{1}{x} \ln \frac{N_0}{N} = \frac{1}{x} \ln \frac{A_0}{A}
\]  

(1)

The experimental values of the LAC for SR and the micro filler were compared to the results obtained from the XCOM software [32,33]. The relative deviation between the two results is calculated by the following:

\[
Dev(\%) = \frac{LAC_{\text{com}} - LAC_{\text{exp}}}{LAC_{\text{exp}}} \times 100
\]  

(2)

While the relative increase between the results of the LAC of the micro and nano fillers are evaluated via the following:

\[
R \cdot I(\%) = \frac{LAC_{\text{nano}} - LAC_{\text{micro}}}{LAC_{\text{micro}}} \times 100
\]  

(3)

The other radiation attenuation parameters are based on the LAC, such as the Half Value Layer (HVL), which represents the thickness needed to reduce the initial intensity to its half value; the Mean Free Path (MFP), which represents the path of the photon inside the sample without any interactions; and the Tenth Value Layer (TVL), which represents the thickness needed to reduce the initial intensity to its tenth value and can be estimated from the following equation [34–36]:

\[
HVL = \frac{\ln 2}{LAC}, \quad MFP = \frac{1}{LAC}, \quad TVL = \frac{\ln 10}{LAC}
\]  

(4)

Figure 3. The experimental setup used to measure the attenuation coefficient.
The efficiency of shielding materials is estimated by an important parameter called the Radiation Protection Efficiency (RPE) and calculated using the following equation [37–39]:

\[
RPE(\%) = \left[1 - \frac{N}{N_0}\right] \times 100
\]  

(5)

3. Results and Discussion

3.1. SEM Results

SEM images of the prepared samples were scanned and showed, in general, a good distribution of Bi\(_2\)O\(_3\) with the SR composite. On the other hand, the distribution of nanoparticles was better than the microparticles, as shown in Figure 4, which means that the SR containing nanoparticles of Bi\(_2\)O\(_3\) has a higher surface area and lower porosity, compared to the same contents of SR containing microparticles of Bi\(_2\)O\(_3\). Additionally, the porosity of SR containing nanoparticles of Bi\(_2\)O\(_3\) is low, which led to an increase in the mechanical and shielding properties.

![SEM images of the prepared samples](image)

**Figure 4.** SEM images of the prepared samples of (a) SR, (b) SR-5m, (c) SR-5n, (d) SR-30m and (e) SR-30n.

3.2. Mechanical Results

In the case of free SR, the mechanical properties (MPs) of SR composites are relatively poor. The MPs of the SR/micro- and nano Bi\(_2\)O\(_3\) composites are plotted in Figure 5A–D. These figures show the variability of tensile strength, Young’s modulus and elongation at break with different concentrations of micro- and nano-Bi\(_2\)O\(_3\) as fillers. The results show that increasing the filler load leads to a significant increase in the tensile strength, Young’s modulus and elongation at break of up to 30 wt%.

The results also show that the addition of nano-Bi\(_2\)O\(_3\) produces a greater increase in tensile strength, Young’s modulus and elongation at break than micro-Bi\(_2\)O\(_3\) with the same percentage. The concentration of the filler was increased to 40%, and the same mechanical properties were studied as before, and it was found that it was less than 30%, and this is what made us conduct a comprehensive study with a maximum of 30% for micro- and nano-Bi\(_2\)O\(_3\) as a filler in the SR. Low mechanical properties at 40 wt% of the filler content is
likely due to the accumulation of filler material in different rubber layers. The hardness was increased with the increase in the filler contents, and this was normal because the addition of filler in the SR leads to an increase in material hardness.

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The results also show that the addition of nano-Bi$_2$O$_3$ produces a greater increase in tensile strength, Young's modulus and elongation at break than micro-Bi$_2$O$_3$ with the same percentage. The concentration of the filler was increased to 40%, and the same mechanical properties were studied as before, and it was found that it was less than 30%, and this is what made us conduct a comprehensive study with a maximum of 30% for micro- and nano-Bi$_2$O$_3$ as a filler in the SR. Low mechanical properties at 40 wt% of the filler content is likely due to the accumulation of filler material in different rubber layers. The hardness was increased with the increase in the filler contents, and this was normal because the addition of filler in the SR leads to an increase in material hardness.

3.3. Shielding Results

In order to obtain the linear attenuation coefficient experimentally, we represented the relation between Ln (I/I$_0$) and the thickness of the samples, according to the Lambert–Beer law. The slope of the straight line is the absolute value of the LAC. We represent the reduction in the intensity of the photons as a function of the thickness for four samples in Figure 6a–d. In this figure, we show the results for the following samples: SR-5m, SR-5n, SR-30m and SR-30n. The other samples have the same trend shown in this figure, so we did not present the data for the remaining samples in Figure 6a–d.

As one can see in this figure, the slope is negative, which implies that the transmission of the photons through the prepared silicone rubber samples decrease with increasing the thickness from 3 to 13 mm. The slope of the rubber silicon sample, SR-5m, is $-0.1502$ at $0.356 \text{ MeV}$, and, as can be seen from Table 2, the LAC for this sample at $0.356 \text{ MeV}$ is $0.1502 \text{ cm}^{-1}$. The LAC values for all the prepared rubber silicon with different amounts of micro- and nano-Bi$_2$O$_3$ is summarized in Table 3.
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Figure 6. Graphical representation of the reduction in the intensity of the photons as a function of the thickness for (a) SR-5m, (b) SR-5n, (c) SR-30m and (d) SR-30n.

Table 2. Linear attenuation coefficient of silicon rubber with different additives (fraction by weight).

| Energy (MeV) | SR-0  | SR-10m | SR-20m |
|-------------|-------|--------|--------|
|             | XCOM  | EXP    | Dev (%)| XCOM  | EXP    | Dev (%)| XCOM  | EXP    | Dev (%)|
| 0.060       | 0.3097| 0.3059 | 1.25   | 0.9620| 0.9464 | 1.65   | 1.7499| 1.7215 | 1.65   |
| 0.081       | 0.2456| 0.2384 | 3.01   | 0.544 | 0.5305 | 2.52   | 0.9042| 0.8860 | 2.05   |
| 0.356       | 0.1354| 0.1351 | 0.25   | 0.171 | 0.1657 | 3.25   | 0.2141| 0.2113 | 1.35   |
| 0.662       | 0.1043| 0.1033 | 0.98   | 0.118 | 0.1154 | 1.85   | 0.1336| 0.1308 | 2.14   |
| 1.173       | 0.0794| 0.0779 | 1.89   | 0.087 | 0.0861 | 0.62   | 0.0954| 0.0952 | 0.28   |
| 1.333       | 0.0744| 0.0728 | 2.11   | 0.081 | 0.0796 | 1.63   | 0.0889| 0.0876 | 1.48   |
In this study, the linear attenuation coefficient (LAC) values of the SR without Bi$_2$O$_3$ and with 5, 10, 20 and 30% Bi$_2$O$_3$ (in micro and nano sizes) were experimentally measured using different radioactive point sources in the energy range varying from 0.06 to 1.333 MeV. Additionally, we theoretically calculated the LAC for the SR with micro-Bi$_2$O$_3$ using XCOM software. The other parameters based on LAC were calculated, such as HVL, MFP and TVL, and tabulated in Table 4.

**Table 3. Linear attenuation coefficient of bulk and nano samples.**

| Energy (MeV) | XCOM | SR-5m | Dev (%) | SR-5n | R.I (%) | XCOM | SR-30m | Dev (%) | SR-30m | R.I (%) |
|-------------|------|-------|---------|-------|---------|------|--------|---------|--------|---------|
| 0.060       | 0.6213 | 0.6085 | 2.11    | 0.6923 | 12.11   | 2.7206 | 2.6749 | 1.71    | 3.4519 | 22.51   |
| 0.081       | 0.3881 | 0.3805 | 1.99    | 0.4254 | 10.55   | 1.3481 | 1.3315 | 1.25    | 1.7538 | 20.08   |
| 0.356       | 0.1525 | 0.1502 | 1.52    | 0.1635 | 8.14    | 0.2672 | 0.2621 | 1.95    | 0.3248 | 15.32   |
| 0.662       | 0.1106 | 0.1083 | 2.15    | 0.1169 | 7.31    | 0.1534 | 0.1496 | 2.54    | 0.1786 | 13.22   |
| 1.173       | 0.0829 | 0.0815 | 1.62    | 0.0876 | 6.88    | 0.1063 | 0.1039 | 2.31    | 0.1182 | 11.46   |
| 1.333       | 0.0775 | 0.0756 | 2.55    | 0.0810 | 6.67    | 0.0987 | 0.0976 | 1.22    | 0.1098 | 11.11   |

The comparison between the experimental and theoretical LAC values for the SR (free Bi$_2$O$_3$) and SR with 20% micro-Bi$_2$O$_3$ is plotted in Figure 7. We notice good comparability between both LAC values measured in the lab and those calculated by XCOM. This is true for most tested energies, however, we found some minor differences between both approaches, and this is acceptable since usually anyone can find some small errors in the experimental part, but generally the experimental results match the XCOM results in an acceptable manner. This is an essential and important step since it provides confidence in the accuracy of the geometry utilized in the lab for the determination of LAC for the SR and SR/micro-Bi$_2$O$_3$ samples. We also calculated the error (Dev.%) between the experimental and XCOM data.

**Table 4. The HVL, MFP and TVL for all the micro and nano prepared samples.**

| Shielding Parameters | Energy (MeV) | SR-0 | SR-5m | SR-5n | SR-10m | SR-20m | SR-30m | SR-30n |
|----------------------|--------------|------|-------|-------|--------|--------|--------|--------|
| HVL (cm)             | 0.060        | 2.2380 | 1.1156 | 1.0012 | 0.7206 | 0.3961 | 0.2548 | 0.2008 |
|                      | 0.081        | 2.8221 | 1.7860 | 1.6294 | 1.2745 | 0.7666 | 0.5142 | 0.3952 |
|                      | 0.356        | 5.1777 | 4.5465 | 4.2399 | 4.0525 | 3.2373 | 2.5943 | 2.1339 |
|                      | 0.662        | 6.6456 | 6.2649 | 5.9318 | 5.8667 | 5.1878 | 4.5185 | 3.8818 |
|                      | 1.173        | 8.7318 | 8.3659 | 7.9165 | 8.0008 | 7.2628 | 6.5214 | 5.8647 |
|                      | 1.333        | 9.3223 | 8.9437 | 8.5600 | 8.5469 | 7.7959 | 7.0193 | 6.3156 |
| MFP (cm)             | 0.060        | 3.2287 | 1.6095 | 1.4444 | 1.0395 | 0.5715 | 0.3676 | 0.2897 |
|                      | 0.081        | 4.0714 | 2.5767 | 2.3507 | 1.8387 | 1.1060 | 0.7418 | 0.5702 |
|                      | 0.356        | 7.3833 | 6.5929 | 6.1169 | 5.8466 | 4.6705 | 3.7428 | 3.0786 |
|                      | 0.662        | 9.5876 | 9.0383 | 8.5577 | 8.5069 | 7.4844 | 6.5188 | 5.6002 |
|                      | 1.173        | 12.5973 | 12.0695 | 11.4212 | 11.5427 | 10.4779 | 9.4084 | 8.4610 |
|                      | 1.333        | 13.4492 | 12.9030 | 12.3495 | 12.3565 | 11.2472 | 10.1267 | 9.1114 |
| TVL (cm)             | 0.060        | 7.4345 | 3.7060 | 3.3259 | 2.3936 | 1.3158 | 0.8463 | 0.6670 |
|                      | 0.081        | 9.3748 | 5.9330 | 5.4126 | 4.2338 | 2.5466 | 1.7080 | 1.3129 |
|                      | 0.356        | 17.0007 | 15.1031 | 14.0846 | 13.4623 | 10.7542 | 8.6181 | 7.0887 |
|                      | 0.662        | 22.0762 | 20.8115 | 19.7049 | 19.5879 | 17.2335 | 15.0102 | 12.8949 |
|                      | 1.173        | 29.0063 | 27.7910 | 26.2982 | 26.5780 | 24.1264 | 21.6636 | 19.4822 |
|                      | 1.333        | 30.9680 | 29.7103 | 28.4357 | 28.4519 | 25.8976 | 23.3176 | 20.9799 |
We found that the Dev.% for SR (free Bi$_2$O$_3$) is confined between 0.25 and 2.55%, while the Dev.% for the SR with 10 micro-Bi$_2$O$_3$ is limited between 0.62 and 3.25%. The Dev.% also ranges between 0.28 and 2.14% for the SR with 20 micro-Bi$_2$O$_3$, while the Dev.% for the SR with 30 micro-Bi$_2$O$_3$ is limited between 1.22% and 2.54%. These results confirm that the Dev.% is small (less than 3%), which reaffirms the compatibility of the practical and theoretical results.

In Figure 8a, we plot the LAC for the SR and the RS with different concentrations of micro-Bi$_2$O$_3$ (5, 10, 20 and 30%). Using this figure, we aim to understand the influence of adding some fractions of Bi$_2$O$_3$ into the SR on the attenuation performance of the prepared samples. Evidently, the lowest LAC is found in the SR and the LAC progressively increases as the amount of Bi$_2$O$_3$ increases from 5 to 30%, where the maximum LAC is reported for the SR + 30% Bi$_2$O$_3$ sample. The reason for this enhancement in LAC is due to the high density and atomic number of bismuth, and it is known that adding high atomic number elements to the materials increases the probability of the interaction between the photons and the electrons in the materials. Consequently, incorporating Bi$_2$O$_3$ into the SR sample leads to the enhancement of the radiation protection performance.

In order to compare the effect of Bi$_2$O$_3$ size on the attenuation performance of the SR, we plotted the LAC for the SR with 5% micro- and nano-Bi$_2$O$_3$ in Figure 8b, and SR with 30% micro- and nano-Bi$_2$O$_3$ in Figure 8c. The LAC values for the SR-5n is higher than the LAC of SR-5m, and the same for 30% (i.e., the LAC for the SR with nanoparticles is higher than micro-Bi$_2$O$_3$). These results imply that the radiation interaction probability increases when the micro-Bi$_2$O$_3$ is replaced with nano-Bi$_2$O$_3$ in the SR. From Equation (3), we define a parameter called relative increase (R.I), which shows the enhancement in the LAC due to the replacement of micro-Bi$_2$O$_3$ by nano-Bi$_2$O$_3$. The R.I is higher than 1, which reaffirms the importance of using nanosized Bi$_2$O$_3$ to develop an effective attenuation barrier (see Figure 8d). Additionally, the RI for 30% of Bi$_2$O$_3$ is higher than that with 5% of Bi$_2$O$_3$. Accordingly, SR with 30% of Bi$_2$O$_3$ has interesting radiation shielding features, compared to the SR with micro-Bi$_2$O$_3$.

Figure 9a,b shows the measured gamma photon transmission through the RS with micro-Bi$_2$O$_3$ and nano-Bi$_2$O$_3$, respectively. We call this T micro and T nano. It can be seen that both T micro and T nano exponentially decrease with increasing the thickness from 3 to 13 mm. In Figure 9a, the T micro is lower than that of SR (free Bi$_2$O$_3$), which means that the transmission of the photons through the sample with Bi$_2$O$_3$ is lower than the transmission of photons through the free Bi$_2$O$_3$ SR sample. This means that the addition of Bi$_2$O$_3$ reduces the transmission of the photons through the prepared silicon rubber.
Additionally, we can see that the T micro depends on the amount of Bi₂O₃ incorporated into the SR. The more Bi₂O₃ in the SR, the lower the T micro. Hence, the incorporation of Bi₂O₃ has a positive influence on the attenuation performance of the SR. If we observe Figure 9b, we can conclude the same results obtained in Figure 9a. In other words, the photon’s transmission through free Bi₂O₃-SR is higher than the SR with nano-Bi₂O₃. This result reaffirms that the increase in the weight fraction of Bi₂O₃ in the SR can efficaciously diminish the photon’s transmittance. Therefore, a high amount of Bi₂O₃ (micro or nano sized) in the SR is a good choice to improve the gamma ray shielding performance for the prepared SR.

In order to understand the influence of the thickness of the prepared SR on the attenuation performance, we plotted the radiation shielding efficiency (RPE) for the SR, SR-5m and SR-30m, in Figure 10a, and SR, SR-5n and SR-30n, in Figure 10b, at the same energy value of 0.081 MeV. In both subfigures, it is evident that the RPE for the SR is less than the RPE for the SR with Bi₂O₃ (micro or nano sized), which reaffirms that adding Bi₂O₃ to the SR causes an improvement in the attenuation performance. Most importantly, we can see that the RPE for the SR with a thickness of 13 mm is higher than that with a thickness of 3 mm. This is correct for the SR incorporating micro- or nano-Bi₂O₃. For instance, from Figure 10a, for the SR-5m, the RPE is 10% and this is increased to 40% for the same sample with a thickness of 13 mm. Therefore, we can conclude that the thickness is an important parameter that affects the attenuation competence of the prepared SR.

Figure 8. The linear attenuation coefficient for the SR (a) with 0, 5, 10, 20 and 30 micro-Bi₂O₃, (b) with 5% of micro- and nano-Bi₂O₃, (c) with 30% of micro- and nano-Bi₂O₃, and (d) the relative increase in the LAC.
high thickness SR is recommended as a good attenuator barrier. Moreover, we found that the RPE for the SR with nano-Bi$_2$O$_3$ is higher than that of the corresponding micro-Bi$_2$O$_3$.

**Figure 9.** The measured gamma photon transmission through the RS with micro-Bi$_2$O$_3$ and nano-Bi$_2$O$_3$, respectively, (a) RS with micro-Bi$_2$O$_3$ at 0.06 MeV, (b) RS with micro-Bi$_2$O$_3$ at 0.662 MeV, (c) RS with nano-Bi$_2$O$_3$ at 0.06 MeV and (d) RS with nano-Bi$_2$O$_3$ at 0.662 MeV.

It is important to compare the radiation attenuation performance for the prepared SR doped with Bi$_2$O$_3$ with a similar material, in order to check the possibility of using these samples in real applications. For this purpose, we compared the half value layer of the SR with 30% of micro- and nano-Bi$_2$O$_3$ with 3 samples: SR 30, 40 and 50% of magnetite iron [40], as shown in Figure 11. We selected one energy value in the comparison, i.e., 0.662 MeV. Evidently, the SR with 30% of Bi$_2$O$_3$ (micro and nano sized) have a lower HVL and thus better attenuation competence than the SR with 30% of magnetite iron. The SR with 30% of micro-Bi$_2$O$_3$ has an HVL of 4.52 cm and this is close to 4.62 cm, which was reported for the SR with 40% of iron. The SR with 30% nano-Bi$_2$O$_3$ is lower than that of the SR with 30 and 40% of iron, but has an almost similar HVL, with the SR being in contact with 50% of the magnetite iron.
Flexible materials were prepared from SR and different sizes of Bi$_2$O$_3$. The morphological, mechanical and shielding properties were determined. The SEM results indicate that the nano filler is significantly better than micro filler. The mechanical results conclude that the flexibility of the materials decreases as we increase the Bi$_2$O$_3$ filler with 30 wt%.

Therefore, the attenuation study was controlled by the flexibility results. The results show good agreement with the theoretical results. The attenuation coefficients of the prepared SR samples showed a clear superiority in lower energy levels over other energies, and the SR’s nano-Bi$_2$O$_3$ was better than the corresponding SR’s micro-Bi$_2$O$_3$ at all discussed energies for the shielding materials.

**Figure 10.** The measured radiation protection efficiency at 3 and 13 mm through (a) the RS with micro-Bi$_2$O$_3$ and (b) nano-Bi$_2$O$_3$ at 0.081 MeV.

**Figure 11.** The HVL of 30% micro and nano prepared samples compared with SR filled with magnetite iron.

### 4. Conclusions

Flexible materials were prepared from SR and different sizes of Bi$_2$O$_3$. The morphological, mechanical and shielding properties were determined. The SEM results indicate that the nano filler is significantly better than micro filler. The mechanical results conclude that the flexibility of the materials decreases as we increase the Bi$_2$O$_3$ filler with 30 wt%. Therefore, the attenuation study was controlled by the flexibility results. The LAC was determined experimentally and the results show good agreement with the theoretical results. The attenuation coefficients of the prepared SR samples showed a clear superiority in lower energy levels over other energies, and the SR’s nano-Bi$_2$O$_3$ was better than the corresponding SR’s micro-Bi$_2$O$_3$ at all discussed energies for the shielding materials.

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References
1. Dong, M.; Zhou, S.; Xue, X.; Feng, X.; Sayyed, M.I.; Khandaker, M.U.; Bradley, D.A. The potential use of boron containing resources for protection against nuclear radiation. Radiat. Phys. Chem. 2021, 188, 109601. [CrossRef]
2. Dong, M.; Xue, X.; Yang, H.; Li, Z. Highly cost-effective shielding composite made from vanadium slag and boron-rich slag and its properties. Radiat. Phys. Chem. 2017, 141, 239–244. [CrossRef]
3. Kamislioglu, M. Research on the effects of bismuth borate glass system on nuclear radiation shielding parameters. Results Phys. 2021, 22, 103844. [CrossRef]
4. Kamislioglu, M. An investigation into gamma radiation shielding parameters of the (Al:Si) and (Al+Na):Si-doped international simple glasses (ISG) used in nuclear waste management, deploying Phy-X/PSD and SRIM software. J. Mater. Sci. Mater. Electron. 2022, 32, 12690–12707. [CrossRef]
5. Gökçe, H.; Öztürk, B.C.; Çam, N.; Andič-Çakır, Ö. Gamma-ray attenuation coefficients and transmission thickness of high consistency heavyweight concrete containing mineral admixture. Cem. Conc. Comp. 2018, 92, 56–69. [CrossRef]
6. Gökçe, H.S.; Yalçınkaya, Ç.; Tuyan, M. Optimization of reactive powder concrete by means of barite aggregate for both neutrons and gamma rays. Constr. Build. Mater. 2018, 189, 470–477. [CrossRef]
7. Mahmoud, M.E.; El-Khatib, A.M.; Halbas, A.M.; El-Sharkawy, R.M. Investigation of physical, mechanical and gamma-ray shielding properties using ceramic tiles incorporated with powdered lead oxide. Ceram. Int. 2020, 46, 15686–15694. [CrossRef]
8. Sayyed, M.I.; Elmahroug, Y.; Elbashir, B.O.; Issa, S. Gamma-ray shielding properties of zinc oxide soda lime silica glasses. J. Mater. Sci. Mater. Electron. 2016, 28, 4064–4074. [CrossRef]
9. El-Nahal, M.A.; El-Khatib, A.M.; Elsafi, M.; Elsafi, M.I.; El-Sharkawy, R.M. Investigation of physical, mechanical and gamma-ray shielding properties of polydimethylsiloxane/bismuth (III) oxide composite for X/Gamma ray shielding. Radiat. Phys. Chem. 2020, 170, 108649. [CrossRef]
10. Mahmoud, M.E.; El-Khatib, A.M.; El-Sharkawy, R.M.; Rashad, A.R.; Badawi, M.S.; Gepreel, M.A. Design and testing of high-density polyethylene nanocomposites filled with lead oxide micro- and nano-particles: Mechanical, thermal, and morphological properties. J. Appl. Polym. Sci. 2019, 136, 47812. [CrossRef]
11. Almurayshid, M.; Alsagabi, S.; Alssalim, Y.; Alotaibi, Z.; Almsalam, R. Feasibility of polymer-based composite materials as radiation shield. Radiat. Phys. Chem. 2021, 143, 109425. [CrossRef]
12. Nagaraja, N.; Manjunatha, H.; Seenappa, L.; Sridhar, K.; Ramalingam, H. Radiation shielding properties of silicon polymers. Radiat. Phys. Chem. 2020, 171, 108723. [CrossRef]
13. Labouriau, A.; Robison, T.; Shonrock, C.; Simmonds, S.; Cox, B.; Pacheco, A.; Cady, C. Boron filled siloxane polymers for radiation shielding. Radiat. Phys. Chem. 2018, 144, 288–294. [CrossRef]
14. Ambika, M.; Nagaiah, N.; Harish, V.; Lokanath, N.; Sridhar, M.; Renukappa, N.; Suman, S. Preparation and characterisation of Isophthalic-Bi2O3 polymer composite gamma radiation shields. Radiat. Phys. Chem. 2017, 130, 351–358. [CrossRef]
15. Karabul, Y.; İçelli, O. The assessment of usage of epoxy based micro and nano-structured composites enriched with Bi2O3 and WO3 particles for radiation shielding. Results Phys. 2021, 26, 104423. [CrossRef]
16. Kameesy, S.; Nashar, D.; Fiki, S. Development of silicone rubber/lead oxide composites as gamma ray shielding materials. Int. J. Adv. Res. 2015, 3, 1017–1023. [CrossRef]
17. Gong, P.; Ni, M.; Chai, H.; Chen, F.; Tang, X. Preparation and characteristics of a flexible neutron and γ-ray shielding and radiation-resistant material reinforced by benzophenone. Nucl. Eng. Technol. 2018, 50, 470–477. [CrossRef]
18. Özdemir, T.; Yılmaz, S.N. Mixed radiation shielding via 3-layered polydimethylsiloxane rubber composite containing hexagonal boron nitride, bismuth (III) oxide for each layer. Radiat. Phys. Chem. 2018, 152, 17–22. [CrossRef]
19. Colas, A.; Curtis, J. Silicone Biomaterials: History and Chemistry & Medical Applications of Silicones. In Biomaterials Science, 2nd ed.; Elsevier Academic Publishing: Amsterdam, The Netherlands, 2004; ISBN 0-12-582463-7.
20. El-Khatib, A.M.; Elsafi, M.; Sayyed, M.; Abbas, M.; El-Khatib, M. Impact of micro and nano aluminium on the efficiency of photon detectors. Results Phys. 2021, 30, 104908. [CrossRef]
21. Abbas, M.I. Validation of analytical formulae for the efficiency calibration of gamma detectors used in laboratory and in-situ measurements. Appl. Radiat. Isot. 2006, 64, 1661–1664. [CrossRef][PubMed]
22. Abbas, M.I. A new analytical method to calibrate cylindrical phoswich and LaBr3(Ce) scintillation detectors. Nucl. Instrum. Methods Sect. A 2010, 621, 413–418. [CrossRef]
26. Elsafi, M.; El-Nahal, M.A.; Sayyed, M.I.; Saleh, I.H.; Abbas, M.I. Effect of bulk and nanoparticle Bi$_2$O$_3$ on attenuation capability of radiation shielding glass. Ceram. Int. 2021, 47, 19651–19658. [CrossRef]

27. Eid, M.S.; Bondouk, I.I.; Saleh, H.M.; Omar, K.M.; Sayyed, M.I.; El-Khatib, A.M.; Elsafi, M. Implementation of waste silicate glass into composition of ordinary cement for radiation shielding applications. Nucl. Eng. Technol. 2021, in press. [CrossRef]

28. Elsafi, M.; Sayyed, M.; Almuqrin, A.H.; Gouda, M.; El-Khatib, A. Analysis of particle size on mass dependent attenuation capability of bulk and nanoparticle PbO radiation shields. Results Phys. 2021, 26, 104458. [CrossRef]

29. El-Khatib, A.M.; Abbas, M.I.; Elzaher, M.A.; Badawi, M.S.; Alabsy, M.T.; Alharshan, G.A.; Aloraini, D. Gamma Attenuation Coefficients of Nano Cadmium Oxide/High density Polyethylene Composites. Sci. Rep. 2019, 9, 16012. [CrossRef]

30. Alabsy, M.T.; Alzahrani, J.S.; Sayyed, M.I.; Abbas, M.I.; Tishkevich, D.I.; El-Khatib, A.M.; Elsafi, M. Gamma-Ray Attenuation and Exposure Buildup Factor of Novel Polymers in Shielding Using Geant4 Simulation. Materials 2021, 14, 5051. [CrossRef]

31. El-Khatib, A.M.; Elsafi, M.; Almutiri, M.N.; Mahmoud, R.M.M.; Alzahrani, J.S.; Sayyed, M.I.; Abbas, M.I. Enhancement of Bentonite Materials with Cement for Gamma-Ray Shielding Capability. Materials 2021, 14, 4697. [CrossRef]

32. Sayyed, M.I.; Albarzan, B.; Almuqrin, A.H.; El-Khatib, A.M.; Kumar, A.; Tishkevich, D.I.; Trukhanov, A.V.; Elsafi, M. Experimental and Theoretical Study of Radiation Shielding Features of CaO K$_2$O-Na$_2$O-P$_2$O$_5$ Glass Systems. Materials 2021, 14, 3772. [CrossRef]

33. Elsafi, M.; Dib, M.F.; Mustafa, H.E.; Sayyed, M.I.; Abbas, M.I.; Alsubaie, A.; Almalki, A.S.A.; El-Khatib, A.M. Enhancement of Ceramics Based Red-Clay by Bulk and Nano Metal Oxides for Photon Shielding Features. Materials 2021, 14, 7878. [CrossRef] [PubMed]

34. Al-Hadeethi, Y.; Sayyed, M.I.; Barasheed, A.Z.; Ahmed, M.; Elsafi, M. Fabrication of Lead Free Borate Glasses Modified by Bismuth Oxide for Gamma Ray Protection Applications. Materials 2022, 15, 789. [CrossRef]

35. Al-Harbi, N.; Sayyed, M.I.; Al-Hadeethi, Y.; Kumar, A.; Elsafi, M.; Mahmoud, K.A.; Khandaker, M.U.; Bradley, D.A. A novel CaO-K$_2$O-Na$_2$O-P$_2$O$_5$ glass systems for radiation shielding applications. Radiat. Phys. Chem. 2021, 188, 109645. [CrossRef]

36. Mhareb, M.H.A.; Zeama, M.; Elsafi, M.; Alajerami, Y.S.; Sayyed, M.I.; Saleh, G.; Hamad, R.M.; Hamad, M.K. Radiation shielding features for various tellurium-based alloys: A comparative study. J. Mater. Sci. Mater. Electron. 2021, 32, 26798–26811. [CrossRef]

37. Aloraini, D.A.; Almuqrin, A.H.; Sayyed, M.I.; Al-Ghamdi, H.; Kumar, A.; Elsafi, M. Experimental Investigation of Radiation Shielding Competence of Bi$_2$O$_3$-CaO-K$_2$O-Na$_2$O-P$_2$O$_5$ Glass Systems. Materials 2021, 14, 5061. [CrossRef]

38. Elsafi, M.; Alrashedi, M.; Sayyed, M.; Al-Hamarneh, I.; El-Nahal, M.; El-Khatib, M.; Khandaker, M.; Osman, H.; Askary, A. The Potentials of Egyptian and Indian Granites for Protection of Ionizing Radiation. Materials 2021, 14, 3928. [CrossRef] [PubMed]

39. Elsafi, M.; Koraim, Y.; Almurayshid, M.; Almasoud, F.I.; Sayyed, M.I.; Saleh, I.H. Investigation of Photon Radiation Attenuation Capability of Different Clay Materials. Materials 2021, 14, 6702. [CrossRef]

40. Buyuk, B. Gamma-Ray Attenuation Properties of Flexible Silicone Rubber Materials while using Cs-137 as Radioactive Source. Eur. J. Sci. Technol. 2019, 15, 28–35. [CrossRef]