Halos around edge-on disk galaxies in the SDSS

Stefano Zibetti$^1$, Simon D. M. White$^1$ and Jon Brinkmann$^2$

$^1$Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Str. 1, D-85748 Garching bei München, Germany

$^2$Apache Point Observatory, PO Box 59, Sunspot, NM 88349, USA

Accepted. Received: in original form 4 June 2003

ABSTRACT

We present a statistical analysis of halo emission for a sample of 1047 edge-on disk galaxies imaged in five bands by the Sloan Digital Sky Survey (SDSS). Stacking the homogeneously rescaled images of the galaxies, we can measure surface brightnesses as deep as $\mu_r \sim 31$ mag arcsec$^{-2}$. The results strongly support the almost ubiquitous presence of stellar halos around disk galaxies, whose spatial distribution is well described by a power-law $\rho \propto r^{-3}$, in a moderately flattened spheroid ($c/a \sim 0.6$). The colour estimates in $g-r$ and $r-i$, although uncertain, give a clear indication for extremely red stellar populations, hinting at old ages and/or non-negligible metal enrichment. These results support the idea of halos being assembled via early merging of satellite galaxies.

Key words: galaxies: halos, galaxies: structure, galaxies: photometry, galaxies: spiral

1 INTRODUCTION

The most commonly accepted paradigm for the formation of structure in the universe, ranging from galaxies to clusters and superclusters of galaxies, predicts that they are assembled via the hierarchical clustering of dark matter (DM) halos, in the framework of the so called ΛCDM cosmology. Although these models have been very successful in describing large scale structure and much recent progress has been made in understanding the processes behind the assembly of individual galaxies through numerical simulations (e.g. Kauffmann, White, 1993; Benson, Cole, Frenk, 1996; Navarro, White, 1994; Sommer-Larsen, Gelato, Vedel, 1999), the ongoing disruption process of the Palomar 5 globular cluster (Kauffmann, Whittaker, 1993; Odenkirchen et al. 2002), and the detection of streams in the MW is typically 7 to 10 magnitudes fainter than the central parts of the other galactic components (disk, bulge) and than the sky. At present day, observations of the halo light and mass must be ascribed to this kind of interactions and how common they were in the past is still unclear. In order to answer these questions in a more general context, observations of the halo are available only for a handful nearby galaxies and provide varying results. Recent work by Ferguson et al. (2002) has demonstrated the presence of substructure in the moderately metal-enhanced spiral halo of M31, that is likely to be the relic of the disruption of one or more small companion galaxy. The search for halos in more distant galaxies, for which stars belonging to different components cannot be resolved, has been focused on edge-on disks, because of the much lower contamination of the halo by the projected disk stars. Problems with flat fielding, scattered light from other background and foreground sources, and extended PSF wings make it extremely difficult to obtain reliable photometry down to 29-30 mag arcsec$^{-2}$, as required in order to characterise galactic halos. After the first detection of halo around NGC 5907 claimed by Sackett et al. (1994),...
many controversial results have followed. The latest and deepest observations of this galaxy (see e.g. Zheng et al. 1997) strongly support the extraplanar emission being instead a ring which results from tidal disruption of a satellite galaxy. In the most complete study so far, (but see Sec. 4 for a more exhaustive review of recent results in the literature), the deep observations of a sample of 47 edge-on galaxies, by Dalcanton & Bernstein (2002), provide evidence for the ubiquitous presence of red envelopes around disk galaxies, which the authors attribute to an old, moderately metal-enriched, thick disk structure.

In this paper we present the results from the statistical study of halo emission from a sample of more than 1000 edge-on disk galaxies imaged by the Sloan Digital Sky Survey (SDSS, York et al. 2000). The SDSS is imaging about a quarter of the sky in the u, g, r, i, and z bands, with 54 sec drift scan exposures at the dedicated 2.5 m Apache Point Observatory telescope (Fukugita et al. 1996; Gunn et al. 1998; Hogg et al. 2001; Smith et al. 2002; Pier et al. 2003), reaching ∼ 25 mag arcsec$^{-2}$ at S/N ∼ 1 for a single pixel. In order to reach a surface brightness as low as 29 mag arcsec$^{-2}$, we adopt a stacking technique, in which the images are combined of all the galaxies. First, the images must be geometrically transformed in order to make the galaxies superposable. Other external sources must then be masked. Finally, the count statistics of each pixel is considered and a suitable estimator is chosen to represent the distribution. In this way it is possible not only to increase the S/N by a factor √1000, but also to remove statistically the major sources of contamination for deep photometry of individual objects, namely foreground and background sources, inhomogeneities in the flat field and light scattered inside the camera.

The paper is organised as follows: the sample is described in Sec. 2. In Sec. 3 we describe the image processing and the stacking procedure. The results are analysed in Sec. 4, paying particular attention to the noise properties of the resulting images and to the possible sources of error and of bias. A discussion, including a comprehensive comparison with previous results in the literature and the possible implications for galaxy formation, is given in Sec. 5. A summary and the conclusions of this work are reported in Sec. 6.

2 THE SAMPLE

As of April 2002 the SDSS has covered ∼ 2000 square degrees both in 5-band imaging and spectroscopy. Blanton et al. (2002) have selected a sample of galaxies from the Main Galaxy Sample (Strauss et al. 2002), also known as ‘Large-Scale Structure Sample 10’ (LSS10), including all sources with average surface brightness within the Petrosian$^1$ radius in r band $μ_r < 17.77$, that have been successfully targeted by the spectroscopic observations (see Blanton et al. 2003, for details about the ‘tiling’ algorithm). We refer the reader to Blanton et al. (2002) for the details of the sample and the regions of the sky covered. For the purposes of this work we selected a subsample of edge-on galaxies from the LSS10 requiring the following conditions to be satisfied:

- Petrosian magnitude ($P_{mag}$) successfully measured at least in the three most sensitive SDSS pass-bands, namely the g, r, and i band;
- $P_{mag, i} ≤ 17.5$;
- isophotal semi-major axis $a > 10$ arcsec in i band;
- isophotal axis ratio $b/a ≤ 0.25$ in g, r and i band.

Images of the 1221 selected galaxies were inspected by eye in order to prune from the sample objects that are unsuitable for stacking. First of all we discarded a few percent of the galaxies whose axis ratios had been clearly underestimated due to some failure in the SDSS PHOTO reduction pipeline. Galaxies showing evidence of interaction with nearby companions, warps or other irregularities were rejected. The absence of nearby bright sources contaminating the background was required as well. The resulting sample is composed of 1047 galaxies, ranging from $-22.5$ to $-16.0$ i-band absolute Petrosian magnitude, in units of mag+5 log h. The redshift distribution of the sample peaks at $z ≈ 0.05$ with a standard deviation of 0.035. Typical physical dimensions range from $1$ to $25$ kpc $h^{-1}$ (Petrosian radius in the i band), with a median value of $7.4$ kpc $h^{-1}$. A summary of the sample properties is reported in Fig. 1. Eye inspection of the single galaxies confirms that our sample is dominated by late-type disk galaxies, with at most a few per cents of Sb-c or Sb. Most of the galaxies appear to be almost bulge-free and the the remainder have quite small ‘classical’ bulges.

3 THE IMAGE STACKING

3.1 The image pre-processing

The raw SDSS imaging data is available as 2048x1489 pixel$^2$ (13.5x9.8 arcmin$^2$) bias subtracted and flat-fielded ‘corrected frames’. Using SExtractor v2.2.2 (Bertin & Arnouts 1996) we accurately determined the centre and the position angle of the major axis for each galaxy. From the segmentation image output by SExtractor we obtain a mask for all the sources in each field detected with S/N ≥ 1. The background level for each galaxy was determined as the mode of the pixel count distribution in an annulus with inner radius $3 × a_{iso,i}$ and outer radius $6 × a_{iso,i}$ (where $a_{iso,i}$ is the isophotal major semi-axis at 25.0 mag arcsec$^{-2}$ in i-band). This background was then subtracted from each image.

1 Petrosian (1976) defines the Petrosian radius as the radius at which the surface brightness equals a given fraction of the average surface brightness inside that radius. The Petrosian flux (and hence the magnitude) is defined as the flux inside a certain number of Petrosian radii. See Stoughton et al. (2002) for the full description of the procedure adopted in the SDSS data reduction and the actual parameters.

2 the SDSS reduction pipeline PHOTO (Lupton et al. 2001) provides an elliptical fit of the 25.0 mag arcsec$^{-2}$ isophote parametrised by the semi-axes a and b
3.2 Photometric scale-lengths

The main hypothesis underlying the stacking technique as a reliable statistical tool to investigate halo properties as an assumed self-similarity of the disk galaxies, or at least of their diffuse component. There must exist a 'characteristic' scale-length, such that after rescaling, all galaxies can be superposed. The validity of this assumption will be discussed in more detail in Sec. 3.3.2.

Since the surface brightness distribution of edge-on disks is affected strongly by dust extinction, we chose the $i$ band ($\lambda_{\text{eff}} = 7480\,\text{Å}$) as the reference pass-band in order to characterise the scale-length of our sample. This choice represents the best trade-off between the need for a high sensitivity and the desire to limit the effects of dust$^3$. Many different scale-lengths can be defined from photometric analysis.

We consider the following four scale-lengths:

- the Petrosian radius $r_{\text{Peto}}$, as obtained from the SDSS photometric database (see Abazajian et al. 2003) and Stoughton et al. 2002
- the effective or half light radius $r_{50}$
- the exponential scale-length $r_{\exp}$
- an isophotal radius obtained from the one-dimensional light profile along the major axis $r_{1D}$

$r_{50}$, $r_{\exp}$ and $r_{1D}$ have been determined using dedicated software developed in the IRAF environment. In order to evaluate the two former parameters, we derive a surface brightness profile from circular aperture photometry extending out to 1.5 isophotal ($\mu_i = 25\,\text{mag arcsec}^{-2}$) radii. $r_{50}$ is then obtained as the radius enclosing 50 per cent of the total flux, while the exponential scale radius $r_{\exp}$ is derived from the least squares fit to the surface brightness profile between $r_{50}$ and $r_{90}$ (i.e. the radius enclosing 90 per cent of the flux).

The basic motivation for analysing an one-dimensional brightness profile, derived by collapsing the image of the galaxy along the minor axis, is to have an estimate of the brightness which is as much as possible independent of the inclination. The surface brightness enhancement is, in fact, important and severely dependent on the inclination, when the edge-on condition is approached. Assuming low or negligible extinction, the quantity $\zeta \equiv -2.5 \log \frac{\text{Flux}(x)}{\text{Flux}(x)}$, where $\text{Flux}(x)$ is the flux enclosed within the projected distance $x$ from the minor axis of the galaxy, is independent both of the inclination and of the distance of the galaxy. As reference for determining $r_{1D}$ we chose $\zeta = 25.0\,\text{mag arcsec}^{-2}$, which corresponds roughly to a surface brightness of $\mu = 25.0\,\text{mag arcsec}^{-2}$ for a typical edge-on galaxy.

All four scale-lengths are quite strongly correlated, as expected for self-similar exponential profiles. The typical scatter around the 1:1 relation between pairs of corresponding scale-lengths is $\sim 15$ per cent.

3.3 The image transformation and stacking

For each of the four scale-lengths considered, the median value in the sample, rounded to an integer number of pixels$^4$, has been taken as reference for the rescaling, as given in Table 1. All galaxy images have been geometrically transformed using the drizzle re-sampling technique (as implemented in the IRAF geotran task) in order to correctly propagate the original noise properties. Each image has been translated to the galaxy centre, rotated according to the measured position angle of the major axis, and expanded or contracted according to the ratio between the reference scale length and the corresponding measured one. The same transformation has been applied to the corresponding mask, and a 'grow radius' of 10 pixels (in the original image size) around each masked pixel has been adopted in order to mask the extended PSF wings of the brightest sources. Since each image has a different photometric calibration and the measured surface brightness of a galaxy is differently affected by Galactic attenuation, depending on its location in the sky, an intensity rescaling is needed as well. The transformation from the original pixel intensity $i$ to the rescaled one $i'$ is given by the following formula:

$$i' = i \times 10^{-0.4(Z_p - Z_{p,\text{ref}} - K \times A\text{irmass - Reddening})},$$

where $Z_p$ and $Z_{p,\text{ref}}$ are the flux calibration zero points of the image and of reference, respectively, $K \times A\text{irmass}$ is the

| Table 1. Median scale-lengths (in arcseconds) and rescaling reference values (in pixel) |
|-----------------------------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $r_{\text{Peto}}$ (arcsec) | $r_{50}$ (arcsec) | $r_{\exp}$ (arcsec) | $r_{1D}$ (arcsec) | $r_{\text{Peto}}$ (pix) | $r_{50}$ (pix) | $r_{\exp}$ (pix) | $r_{1D}$ (pix) |
| 10.07 | 25 | 4.74 | 12 | 3.76 | 10 | 15.50 | 40 |

$^3$ The $z$ band is in fact the red-most one, but its sensitivity is about a factor 2-3 lower than the $i$ band.

$^4$ The pixel scale of the SDSS CCDs is 0.396 arcsec pix$^{-1}$.
airmass correction, and Reddening is the attenuation due to our Galaxy, as given by [Schlegel, Finkbeiner & Davis (1998)]. All the quantities are expressed in magnitudes.

The combination of the transformed and rescaled images has been performed using the `incombine` IRAF procedure. First of all, the masked pixels are rejected. The median of the count distribution of the remaining pixels is then calculated in order to obtain the median image. An average image is calculated as well, after clipping the 16 per cent percentile tails of the count distribution of the unmasked pixels. Adopting the standard approximation for the mode of a distribution

\[ \text{mode} = 3 \times \text{median} - 2 \times \text{average}, \]

we calculate the mode image. The resulting $512 \times 512$ pixel$^2$ images extend much beyond the detected emission from the galaxies and allow us to determine the properties of the background in great detail. A careful comparison between the three statistical combinations shows that, despite of the conservative masking method adopted, the diffuse luminosity of sources other than the considered galaxies can result in significant skewness in the pixel count distribution and in a systematic increase of the sky surface brightness up to 31 mag arcsec$^{-2}$ in $i$-band in the outermost regions of the average frame with respect to the innermost ones, in which contaminating sources are avoided by selection. This systematic effect in the background is almost completely removed in the mode image. In the following, therefore, we will always refer to that one as the resulting stacked image. For each stacked image the residual background level is determined as the count mode in an annulus of 130 pixel inner radius, 96 pixel thick, and subtracted.

In Fig. 2 we present the images for the four most sensitive pass-bands ($g$, $r$, $i$, $z$), obtained by stacking the images rescaled according to the galaxy exponential scale length. For the $u$ band the signal-to-noise is not sufficient to say anything about the presence and the characteristics of halo emission, therefore we will neglect this band in the following analysis and discussion. Rescaling according to the other scale-lengths does not change the resulting images significantly, as we will demonstrate more quantitatively later on, and therefore they are not shown here. Intensity levels in Fig. 2 are coded in square-root transformation grey scale, suitably adjusted to show the maximum extension of the low surface brightness envelope. We superpose isophotal contours in two magnitude ranges: black contours, corresponding to the faintest isophotes, are obtained adopting a boxcar smoothing scale of $10 \times 10$ pixel, whereas the white, brightest ones, have been calculated with a $2 \times 2$ pixel smoothing scale. The represented isophotal levels are given in the figure caption. The images and the superposed isophotes show very clearly the presence of a diffuse luminous envelope around the disk, in all four considered bands. This halo (whatever physical meaning we give to this word) is particularly evident and round in the $r$ and the $i$ bands, whereas it is significantly flattened in the $g$ and $z$ bands (but the lower sensitivity in the latter band does not allow us to say much).

4 THE ANALYSIS

In this section we present the results of an analysis of the stacked images in the $g$, $r$, $i$, and $z$ pass-bands. We mainly concentrate on the stacking of the complete sample (1047 galaxies), because of the resulting higher sensitivity, but we also consider the stacking of three subsample of bright, intermediate and low luminosity flat galaxies (Sec. 4.4), in order to better understand the possible dependence of the observed halo properties on total luminosity. After analysing the background properties of the stacked images in order to assess our detection limits (Sec. 4.1), the photometric properties are investigated by means of radial sector-averaged surface brightness profiles (Sec. 4.2), and compared to different models of luminosity distributions, namely thin+thick disks and disk+halo (Sec. 4.3). The average halo colours are presented in Sec. 4.4. Unless otherwise specified, we will always use the stacking of the images rescaled according to the exponential disk scale-length. We devote an entire paragraph in Sec. 4.2 to demonstrate that the adopted scale-length is not critical in determining the characteristics of the observed halos.

4.1 The background noise properties

Since our photometric measurements are performed by integrating the flux over different image areas, as will be explained in Sec. 4.2, it is crucial to determine the noise properties on different scales. The presence of large-scale fluctuations is already obvious from a superficial inspection of the contour plots in Fig. 2. We restrict the analysis of the noise to the annulus (130 pixel inner radius and 96 pixel thickness) on which the sky level has been computed, and we consider the rms of the intensity after re-binning the image by different linear factors, ranging from 1 to 50. The dependence of the $\text{rms}$ on the scale-length $L$ is well described by a power law of the form

\[ \text{rms}(L) = \text{rms}_0 L^{-\alpha}, \]  

where $\text{rms}_0$ is the noise on one-pixel scale, and $\alpha \approx 0.7 \rightarrow 0.8$, thus indicating that the noise has significant large scale structure in excess to what is expected in the case of pure Gaussian noise (for which $\alpha = 1$).

4.2 The surface brightness profiles

The most obvious way to investigate the properties of the approximately round, low surface brightness structures emerging in Fig. 2 is to extract surface brightness (SB) profiles, averaging the flux in large wedges at different position angles. First of all, we divide the image in four circular sectors of 60° aperture, centred at 0°, 90°, 180° and 270° position angles (PAs). Each of these sectors is in turn radially divided into a number of coronae, geometrically spaced such that the outer radius of the kth corona is given by $r_k = r_0 \cdot 1.15^k$, with $r_0 = 6 \text{ pixel} = 0.6 r_{\text{exp}}$. Finally, we estimate the mean SB as a function of the radius for 0° (i.e. along the disk) and 90° PA (i.e. perpendicular to the disk) averaging the SB in pairs of corresponding coronae in the two symmetric sectors at 0° and 180° and at 90° and 270° PA, respectively. In each of the four graphs of Fig. 4 we show the SB profiles for the $g$, $r$, $i$, 

---

c⃝2003 RAS, MNRAS
Figure 2. The images resulting from the stacking of the galaxies rescaled according to their exponential scale length, in $g$, $r$, $i$, and $z$ band. Intensity is coded in grey levels through a square root transformation, adopting arbitrary bias and contrast. The overplotted isophotal levels are as follows: 30.0, 29.0, 28.0, 26.0, 24.0, 22.0 for the $g$ and the $r$ band; 29.5, 28.5, 27.5, 25.5, 23.5, 21.5 for the $i$ band; 28.0, 27.0, 26.0, 24.0, 22.0 for the $z$ band. See text for the details. The scales indicate the offset from the galaxy centre in pixel. 10 pixel= $r_{\text{exp}}$.

and $z$ images respectively, in linear scale (upper left panel) and logarithmic scale (upper right panel): open circles represent the 0° PA profile, filled triangles the 90° PA. The shaded areas represent the level of the rms background fluctuations at the scale length corresponding to the area of the coronae in which the SB is averaged, as calculated in the previous section. Thus the $1-\sigma$ detection limits for the SB profiles can be assessed as $\sim 31 \text{ mag arcsec}^{-2}$ for the $g$, $r$, and $i$ band and as $\sim 28 \text{ mag arcsec}^{-2}$ for the $z$ band.

In order to evaluate the errors on the SB we must consider contributions from 1) the background fluctuations and 2) the intrinsic scatter in the average signal from a galaxy. The first one is just provided by the background rms as evaluated in the previous section using Eq. 1 with $L$ given by the square root of the area of the corona over which the
Figure 3. The SB profiles in g, r, i, and z band, in 60° wedges along the disk (PA=0°, open circles) and perpendicular to it (PA=90°, filled triangles). Distances from the centre in pixels (10 pixels corresponding to 1 rexp) are shown in linear scale (left panels) and logarithmic scale (right panels). The sky rms is represented by the shaded areas. Dashed lines represent the 'pure' disk profile at r > 20 pix, obtained as explained in the text. The bottom panels of each graph show the b/a axial ratio of the isophotes as a function of the major axis a.

The estimation of the intrinsic scatter contribution is much more cumbersome, since the shape of the statistical distribution of the pixel counts in the coronae is not known a priori and the light distribution of the galaxy itself is likely to give a major contribution to the rms of the count statistics. In order to remove it, for each pixel we consider the deviation from the average intensity of the corresponding pixels in the four image quadrants, which are symmetric with respect to the x and y axes, and express the intrinsic rms as:

$$rms_{\text{intrinsic}} = \sqrt{\frac{1}{3N} \sum_{i=1}^{N} \sum_{j=1}^{4} \left[ I_{ij} - \langle I_{ij} \rangle \right]^2}$$  \hspace{1cm} (2)$$

where $I_{ij}$ is the pixel intensity, $N$ is the number of pixels per corona per quadrant, and $\langle I_{ij} \rangle$ is the average intensity over the $j$ index. In the absence of any large scale background fluctuation the error on the average intensity is just obtained dividing the (2) by $\sqrt{4N}$. Adding the contribution of the large scale fluctuations, we can write the error as:

$$\sigma = \sqrt{\frac{(rms(L))^2}{2} + \frac{rms_{\text{intrinsic}}^2}{4N}}$$ \hspace{1cm} (3)$$

where $rms(L)$ is given by Eq(1) with $L$ given by the square root of the area of the corona, and the factor 2 comes in from having averaged two coronae. Such an error estimate has been proved to be consistent with the scatter of the average
intensity in the corresponding coronae in the four quadrants.

In the lower panels of each graph in Fig. 3 we plot the axial ratio $b/a$ of the isophotes as a function of the radius (semi-major axis). This is calculated as follows. We assign a number of SB levels and determine the radius $r$ at which such SB’s are reached at different PAs $\theta$, by interpolating the SB profiles extracted from 6 wedges per quadrant. Assuming $r = r(\theta)$ is well represented by an ellipse with the major axis along the $x$ direction, we derive the best fitting semi-axes $a$ and $b$ by means of a standard least squares algorithm.

As it is apparent from the straight-line behaviour of the open circles in the linear-scale plots of Fig. 3, the profile of the wedges centred on the disk show an exponential decrease of the SB with radius, as it is typical for disks. Perpendicular to the disk, instead, the rapid initial decrease of the SB becomes shallower as we go further away from the centre of the galaxy. The trend is well approximated by a power-law with index $\sim 2$, as the straight-line behaviour of the triangles in the log-scale plots points out. This is in general true for the four bands analysed. However, the relative intensity at the same radial distance along the disk and perpendicular to it is different in different bands, reflecting a possible dependence of the flattening of the diffuse halo on the band and, in turn, this points to colours gradients in the halo itself. As already noted from the isophotal contours in Fig. 2, the halo is prominent in the $r$ and the $i$ band, reaching a SB comparable to that of the disk at $r \sim 8 - 10 \ r_{\text{exp}}$ and making the isophotal shape significantly rounder ($b/a \sim 0.5 - 0.6$). In the $g$ band the halo has very little extension (the surface brightness drops below 31 mag arcsec$^{-2}$ beyond $\sim 4 \ r_{\text{exp}}$), thus leaving the isophotes extremely flattened. For the $z$ band the measurements are inconclusive: there is some hint of a shallowing of the slope of the profile, but the $S/N$ drops below 1 already at $\sim 3 \ r_{\text{exp}}$ at the level of 28.5 mag arcsec$^{-2}$.

In Fig. 3 for $r > 20$ pix, we also show as dashed lines the ‘pure disk’ profiles obtained subtracting the $90^\circ$ profile from the $0^\circ$ profile, after stretching the former by a factor $0.6^{-1}$ to take the flattening of the halo into account (see Sect. 4.3 for details on the 0.6 factor). There is evidence that the ‘pure’ disk slope steepens beyond $4 - 5 \ r_{\text{exp}}$ in the $r$ and $i$ bands, consistent with studies of individual disks in the literature (see e.g. van der Kruit 2001, Kregel, van der Kruit & de Grijs 2002, and references therein), whilst the results are unclear in the $g$ and $z$ bands.

In order to rule out scattered light and the extended wings of the point spread function (PSF) as major contributors to the observed halos, we have performed the same stacking procedure on the images of stars taken from the same frames as the galaxies to generate effective PSF’s in each band. In each frame we identify a star 1) whose central brightness differs by less than 2 mag arcsec$^{-2}$ from the central SB of the galaxy and 2) which is distant from other contaminating sources, as requested for the galaxy selection. Then, sources other than the star are masked, the frame is re-centred on the star and the same geometrical transformations as applied to the galaxy are performed. The radial profile of the PSF can be reproduced by a Gaussian core plus exponential wings over a large extension. Fig. 4 shows the analytic fit to the measured PSF’s in the four bands, expressed as the difference of magnitude with respect to the central surface brightness. The decline in the core is very sharp, $6 - 7$ mag arcsec$^{-2}$ within 5 pixel, and the exponential wings contribute less than $1/10^4$ of the central surface brightness at radii larger than 20 pixels. We will analyse the effects of the PSF on the measured profiles in the next section, by convolving with different models for the light distributions.

The characteristics of the observed halo profiles show little or no dependence on the scale-length adopted for rescaling the images of the galaxies. In Fig. 5 we plot the SB profile in the $90^\circ$ PA wedge in the four bands, using different symbols for the different rescalings: open circles for $r_{\text{exp}}$, filled triangles for $r_{\text{Petro}}$, open squares for $r_{\text{iso1D}}$ and filled circles for $r_{\text{Petro}}$. The $r$ coordinate of each point is exactly rescaled in order to match the sample median values of the four scale-lengths considered. As in Fig. 4 the shaded areas represent the sky rms. The error-bars are calculated as explained before. The agreement between the different rescalings is extremely good: almost all points are consistent within the error-bars, with a handful of exceptions for the $r_{\text{iso1D}}$ rescaling. Even for these, the deviation is less than 3 $\sigma$. Thus we conclude that there is no systematic dependence of the average halo properties on the profile shape of the disk as described by variations in relative scale-lengths.

![Figure 4. The PSF profiles in g (solid line), r (dotted line), i (short-dashed line), and z band (long-dashed line), expressed as difference of magnitude with respect to the central surface brightness. The lines represent the analytic fit (Gaussian core plus exponential wings) to the radial profile measured on the stacked image of stars, as explained in the text.](image)
In this section we investigate the structural properties of the detected emission by means of simple models of the light distribution. In particular, we consider the possible contribution from a thick disk component, with an exponential vertical light density distribution, and from a (moderately) flattened power-law halo. Making predictions from models of this kind is non-trivial and must take into account that the observed emission results from a double convolution of the ‘true’ average light density distribution of the galaxies with 1) the distribution of inclinations and 2) the effective PSF, as computed above. The models are calculated as follows. First we assume a particular 3-dimensional distribution of light. We produce a set of 1000 Monte Carlo realizations of the projected surface brightness, uniformly varying the inclination angle of the disk between 0 and 15 degrees (roughly corresponding to a projected axial ratio between 0 and 0.25 for an infinitely thin disk, as required by the sample selection criterion for the galaxies). The 1000 realizations are then averaged and convolved with the analytic PSF computed in the previous section, separately for each band. We do not expect to reproduce the stacked images near the nucleus nor at small distances from the disk plane, because we do not model dust extinction. Thus we compare our models to the observations by means of vertical-cut profiles, that allow us to exclude these ‘forbidden’ regions. In each cut, whose width is chosen to be proportional to the distance from the minor axis of the image, we average the flux coming from the four quadrants.

Figure 5. The surface brightness profiles in g, r, i and z band, at 90° PA, for different adopted rescalings. Open circles refers to images rescaled according to \( r_{\text{exp}} \), filled triangles to \( r_{\text{iso}} \), open squares to \( r_{\text{iso1D}} \) and filled circles to \( r_{\text{Petro}} \). The sky rms is represented by the shaded areas.

4.3 Modelling the halo
In the thin+thick disk model the 3-dimensional light density of each individual galaxy is assumed to be given by:

$$\nu(r, z) = N e^{-r/r_{\text{exp}}} \left[ e^{-z/a_{\text{thin}}} + R_{\text{thick}}^2 e^{-z/a_{\text{thick}}} \right]$$

where $N$ is the normalisation factor, $R$ is the flux ratio of the thick over the thin disk, $r_{\text{exp}}$ is the exponential scale-length of the radial SB distribution, $z_{\text{thin}}$ and $z_{\text{thick}}$ are the exponential vertical scale-lengths of the thin and thick disks respectively. We fix $r_{\text{exp}} \equiv 10$ pixels, and $z_{\text{thin}} \equiv 1$ pixel. No disk truncation is adopted. The realizations cover a logarithmic spaced grid of four by four values in the $z_{\text{thick}} - R$ parameter space ($z_{\text{thick}}$ ranging from $10^{-2}$ to $10^{0.8}$ pixels, $R$ from 0.01 to 0.4). The normalisation $N$ is left as a free parameter and fitted by minimising the $\chi^2$. We find that the thin+thick disk models fail to reproduce the observed SB distribution of the observed halos, since they predict a sharp exponential cut-off of the SB along the $z$ coordinate, which is inconsistent with the observed power-law profile.

In the disk+halo models, we assume a halo component with a generalised Hubble density distribution as introduced by Elson, Fall & Freeman (1985), modified to allow the iso-density surface to be oblate spheroids:

$$\nu_{\text{halo}}(r, z) \propto \left[ 1 + \frac{r^2 + \frac{z^2}{c/a} - \xi}{r_{\text{exp}}^2} \right]^{-\frac{(\xi+1)/2}{2}}$$

where $c/a$ is the flattening parameter, $r_{\text{exp}}$ is the softening parameter or core radius, and $\xi$ is the power-law index of the projected SB. The disk component is modelled by a double exponential distribution in $r$ and $z$, without any truncation:

$$\nu_{\text{disk}}(r, z) \propto e^{-r/r_{\text{exp}}} \cdot e^{-z/z_{\text{exp}}}$$

with $r_{\text{exp}}$ and $z_{\text{exp}}$ representing the exponential scale lengths in $r$ and $z$ respectively. We fix $r_{\text{exp}} \equiv 1$ pixel and $z_{\text{exp}} \equiv 10$ pixels, and realize a grid of models in the parameter space ($z_{\text{exp}}$ ranging from $10^{-2}$ to $10^{0.8}$ pixels, $R$ from 0.01 to 0.4). The normalisation $N$ is left as a free parameter and fitted by minimising the $\chi^2$. The best fitting models for the $g$, $r$, and $i$ band are presented in Fig. 6. For each band we plot the vertical SB profiles at four different distances from the centre of the galaxy, as obtained in the vertical cuts described above, offset by 1 mag arcsec$^{-2}$ one from the other. Even if the $\chi^2$ are extremely high, thus demonstrating that the adopted models cannot reproduce in the details the complexity of the galaxy structure, the general agreement with the measured points is satisfactory and we are successful in reproducing the trend of the profiles. Besides the total model profiles (heavy lines), we plot also the exponential disk components alone (light lines): while dominating at small height, they give negligible contribution at $z \geq 30$ pixels ($3 r_{\text{exp}}$). The best fitting model parameters are reported in the panels of Fig. 6. The disk scale-height is quite well constrained to $h \sim 1.5 r_{\text{exp}}$. The power-law slope ($\xi$) is steeper in $g$ band (2.50), and increasingly shallower in $r$ and $i$ (2.00) and $z$ band (1.50), while the halo shapes get increasingly rounder from $c/a = 0.50$ in $g$, to 0.60 in $r$ and $i$, and 0.70 in $z$ band. This is in good agreement with the previous analysis on the images themselves and on the radial profiles. The surface brightness of the halo component at $r = r_{\text{exp}}$ along the minor axis is 25.84, 25.82, 25.03 and 25.26 mag arcsec$^{-2}$ in the $g$, $r$, $i$ and $z$ band respectively. We can estimate the amount of halo light coming from outside the 25 mag arcsec$^{-2}$ isophote as $\sim 2 - 3$ per cent of the total galaxy light.

The models derived above allow us to quantify the pollution of the outer envelope by scattered light and PSF wings. We note that, at $r = 20$ pix, the PSF-convolved disk component contributes $\sim 30$ per cent of the total surface brightness. This contribution decreases very rapidly at larger distances, and becomes negligible at $r > 30$ pix in all the bands. We conclude that scattered light from the disk contributes much less than 30 per cent of the total (disk+halo) measured light beyond 20 pixel.

4.4 The halo colours

Based on the SB profiles presented in Sec. 4.2, we derive the colour profiles in the two 60$^\circ$-aperture sectors including the disk and perpendicular to it. We concentrate on the $g - r$ and $r - i$ colours, excluding colours involving the $z$ band, because of its lower sensitivity. In Fig. 7 the dots represent the colours measured perpendicular to the disk, with the error-bars derived from the errors on the SB profiles; for comparison, with the dotted lines we plot the colour profiles for the disk. This has a bluing gradient toward the outer parts, which is particularly evident for $g - r$, but it is still clearly apparent in $r - i$. Disk colours ($g - r = 0.7 - 0.5, r - i = 0.4$) are consistent with typical star-forming galaxies, once we allow for significant dust extinction, as expected for edge-on conditions. The increasing presence of dust near the galaxy centre and age and metallicity gradients in the disk can also easily explain the observed gradients. Beyond $4 - 5 r_{\text{exp}}$ there is evidence for colours getting redder, possibly indicating that the halo is overtaking the disk. This is consistent with the steepening of the profiles of the ‘pure disk’, shown as dashed lines in Fig. 8.

The $g - r$ profile perpendicular to the disk is extremely noisy: no clear trend can be established and the measurements are definitely unreliable beyond 20 pixels. The halo in these bands is roughly as red as the inner parts of the disk. The $r - i$ colour shows instead a clear reddening toward the outskirts of the galaxy, reaching extremely red colours $\sim 0.8$, about 0.4 mag redder than the disk. We derive the best estimate of the halo colours using the mean colour around 20 pixels and consider the uncertainties given both by the error bars and by the scatter of the points around an ‘ideal’, smooth profile:

$$g - r = 0.65 \pm 0.1$$

$$r - i = 0.60 \pm 0.1$$

These results are not corrected for the effects of the PSF. Based on the analysis in the previous section, we estimate that the SB at $r = 20$ pixel is polluted by scattered light from the inner parts by up to $\sim 30$ per cent. However, this

---

5 The core radius is introduced only for mathematical convenience, to avoid the central divergence of a pure power law.

6 20 per cent in the $g$, 33 per cent in the $r$ and the $i$, and 40 per cent in the $z$ band.
contribution is very similar in all the bands (20 per cent in the \( g \), 33 per cent in the \( r \) and the \( i \) bands) and can red- den the real halo colours by some hundredths up to 0.2 mag (worse case for \( g - r \)). It is worth stressing that this as- sessment has large uncertainties, due to the very simplistic nature of the models here adopted and to their extreme sen- sitivity to the fitting parameters (e.g., changing the vertical scale-length of the disk affects very slightly the goodness of the fit, but can significantly change the disk and scattered light contributions to the colours at 20 pixels).

The robustness and the significance of the estimates given above, will be discussed in detail in Sec. 5.

4.5 Dependence on the total galaxy luminosity

In order to understand the dependence of the halo features on the galaxy luminosity, we analyse the stacked images (exponential scale-length rescaling) for three luminosity bins in the \( i \) band, namely the ‘bright’ \(( -22.5 < i_{\text{abs}} + 5 \log h \leq -20.2 )\), the ‘intermediate’ \((-20.2 < i_{\text{abs}} + 5 \log h \leq -19.0 \)\) and the ‘faint’ one \(-19.0 < i_{\text{abs}} + 5 \log h \leq -16.0 \). The profiles at 0\(^{\circ}\) and 90\(^{\circ}\) PA (obtained as in Sec. 4.2) are plotted in Fig. 8. Open triangles for the ‘faint’ bin, filled squares for the ‘intermediate’, and open circles for the ‘bright’. The solid lines running through the points are the profiles as ob-}

5 DISCUSSION

The analysis performed in the previous section provides strong evidences for the generalised presence of a dif- fuse, low-surface brightness stellar component around disk galaxies. By stacking more than 1000 images, we are able to extract reliable photometry at SB level as faint as \( \sim 31 \text{ mag arcsec}^{-2} \) in the \( g, r \) and \( i \) band and \( \sim 28 \text{ mag arcsec}^{-2} \) in the \( z \) band.

It is worth stressing that the statistical estimator adopted in this work to compute the combined images is extremely
The stacked SB profiles in $g$, $r$, $i$ and $z$ band, at $0^\circ$ (upper curves) and $90^\circ$ PA (lower curves), for three luminosity bins: open triangles represent the ‘faint’ bin, filled squares the ‘intermediate’ and open circles the ‘bright’ one. The solid line is the all-sample profile. The shaded area is the rms background fluctuation.

Figure 8. The stacked SB profiles in $g$, $r$, $i$ and $z$ band, at $0^\circ$ (upper curves) and $90^\circ$ PA (lower curves), for three luminosity bins: open triangles represent the ‘faint’ bin, filled squares the ‘intermediate’ and open circles the ‘bright’ one. The solid line is the all-sample profile. The shaded area is the rms background fluctuation.

robust. The evaluation of the mode for each pixel in the composite image as $3 \times \text{median} - 2 \times \text{average}$, with the average calculated over the count distribution after rejecting the 16 per cent percentile tails and the masked pixels, is effective in removing outliers and spurious contributions from other sources, and in correcting for the skewness of the distribution, while reducing the noise of the standard mode estimation.

The isophotal contours superposed to the images in Fig. 4 show the presence of luminous halos whose shape is clearly rounder than the highly flattened central disk. The shape of the effective PSF, obtained from the stacking of 1000 stars selected from the same frames and with similar criteria as the galaxies, after applying the same geometrical transformations, is not consistent with scattered light and extended PSF wings giving a major contribution to the light detected in the halo. Comparisons with the light distribution expected from simple thin+thick disk models, in which we have accounted for the whole range of galaxy inclinations and for the effective PSF, demonstrate that no exponential vertical disk component can yield the observed power-law shape of the SB profiles at $r > 4 r_{\text{exp}}$ in any of the four considered bands. Adding a moderately flattened ($c/a \sim 0.6$), power-law ($I \propto r^{-2}$ or $\rho \propto r^{-3}$) halo component to a simple exponential disk, it is possible to reproduce the basic features in the observed profiles quite well.

It could be argued, that the emission we detect in the outer regions is produced by small bulges. However, MacArthur, Courteau & Holtzman (2003) have shown that the bulges of disk-dominated galaxies, like the ones in our sample, are in general well represented by ex-
of the spheroidal halo $c/a \sim 0.6$, which is also consistent with the findings in this work. Comparisons with analogous studies of external galaxies are in general difficult. Although its small distance makes M31 the easiest target for observing of the halo population of a disk galaxy, the prominence of its bulge makes it hard to disentangle the density distribution of the halo so that it is perhaps more appropriate to talk about a generic spheroid. Pritchett & van den Bergh (1994) measured the SB of M31 spheroid to $\mu_V \sim 30$ mag arcsec$^{-2}$ and concluded that it can be modelled either by a de Vaucouleurs law or, in its outer parts, by a power-law $\rho \propto r^{-3}$, which is much steeper than what we find. However, the globular cluster distribution follows $\rho \propto r^{-3}$ (Racine 1991) and there is evidence for a shallower power-law index in the outer parts of the halo from more recent observations (Irwin, private communication).

Recent observations of the red giant stars of the nearby, late-type spiral M33 (Ferguson et al. 2003, in preparation), seem to exclude the presence of a spheroidal component around this galaxy, but its nearly face-on aspect makes it difficult to draw firm conclusions.

Results from more distant galaxies are even more uncertain, because of the overwhelming difficulties in going deeper than 28 mag arcsec$^{-2}$. After the first claim by Sackett et al. (1994) of the detection of halo emission from NGC5907, many discrepant measurements have been made by different groups in bands from the optical to the NIR (see e.g. Barnaby & Thronson 1994; Lequeux et al. 1998; Rudy et al. 1997; James & Casali 1998; Lequeux et al. 1998). The latest observations by Zheng et al. (1999) with intermediate-band filters, and by Yost et al. (2000) in optical and NIR, together with the RGB star counts derived by Zepf et al. (2000) from NICMOS observations, seem to rule out the presence of a halo, favouring instead a luminous ring produced by the tidal disruption of a dwarf companion.

However, despite the non-detection of any diffuse component in the Scd galaxy NGC 4244 by Fry et al. (1999), probably because of the low sensitivity of their observations ($\mu_R < 27.5$ mag arcsec$^{-2}$), many studies during the last years support the idea of a luminous envelope (thick disk or halo) surrounding many disk galaxies. Morrison et al. (1997) detected thick disk emission from NGC 891; Abe et al. (1999) have measured $R$ and $I$ light excesses with respect to an exponential disk model in the Scd galaxy IC 5249; Wu et al. (2002) have observed NGC 4565 at 6600A obtaining good accuracy photometry as faint as $\mu = 27.5$ mag arcsec$^{-2}$ and found a halo component with power-law $r^{-2.3 \pm 0.4}$. Similar results are found by Rauscher et al. (1998) in the NIR K band for ESO 240-G11 (power-law halo $\rho \propto r^{-3}$). After observing a sample of 47 extremely flat galaxies in $B$, $R$ and $K_s$ down to extremely faint SB, Dalcanton & Bernstein (2002) have claimed the ubiquitous presence of red stellar envelopes around disk galaxies. It is not clear whether these envelopes extend to a spheroidal halo or are just thick disks, as the authors claim, because their detection limits are just at the surface brightness where we start to see our power-law halo component unambiguously.

In order to establish the origins of these stellar populations, very precise colour measurements are needed. Due to the

![Figure 7](image-url)
Halos around edge-on disk galaxies in the SDSS

enormous observational difficulties, reliable colour measurements of the halos around disks are very scarce: excluding the MW, M31 and M33 for which colour-magnitude diagrams of halo stars and globular clusters can be obtained, the only optical colours available to now are the ones derived by Lequeux et al. (1998) for NGC 5907. Beside these, Dalcanton & Bernstein (2002) have measured \( B - R \) and \( R - K_s \) for the thick disks in their sample. The colours we derived in Sec. 4.4 are, in fact, very uncertain, both because of the intrinsic error of the measurements and because of the practical impossibility to avoid contributions from the disk component. The analysis in Sec. 4.4 showed that scattered light from the disk component is likely to affect the colours by a few hundredths of a mag, but colour excesses up to 0.2 mag cannot be ruled out. If we trust these results \( g - r = 0.65 \pm 0.1, r - i = 0.60 \pm 0.1 \), we find that halos are made of stars which are only marginally \( (2\sigma) \) consistent with old, moderately metal-poor stellar populations. In Fig. 9 we compare the stacked halo \( g - r, r - i \) colours with different data taken from the literature\(^7\). Our point (open circle with error bars) is almost inconsistent with the colours of the MW globular clusters (filled circles, from Harris 1996), being much redder in \( r - i \), and as red as the metal-rich tail of the globular cluster distribution in \( g - r \). We have highlighted 47 Tucanae in the plot (starred dot), because its integrated colours are very similar to M31’s halo. Its \( g - r \) is about the same as our measurements. We note that \( g - r \) is also consistent with the blue end of the elliptical sequence as derived from the SDSS at the median redshift of the sample \( z = 0.05 \) (filled square, Bernardi et al. 2004), and from the observations in Virgo and Coma by Gavazzi et al. in B and V, as given in GOLDMiNe (Gavazzi et al. 2003), whose interquartile range is represented by the back-shaded area. Reasonable agreement is found with the optical colours \( B - R \) derived by Dalcanton & Bernstein (2002) for their thick disks (whose range is represented by the shaded area in Fig. 9). Reconciling the measured \( r - i \) colour with any known stellar population is almost impossible, even if we allow for an extreme 0.1 mag reddening caused by the PSF, as discussed in Sec. 4.4. It is however interesting to note that the colours derived for NGC 5907 by Lequeux et al. (1998) are consistent with ours, but nonetheless troublesome. We exclude significant dust reddening for two reasons. First, the unusually red colour in our data is \( r - i \), despite the fact that dust mostly affects optical/blue bands. Second, in the \( r - i \) profile there is quite strong evidence for a red gradient toward the outer parts, whereas it is known that the dust is concentrated in a thin layer in the disk. Thus we conclude that there is evidence for the halos being made of extremely red stellar populations. This is likely to be primarily due to an old age, but other effects, such as high metallicity or ‘exotic’ low-mass dominated IMF, would be required in order to explain the unusually high \( r - i \).

Our red colours seem to exclude the possibility that the majority of the halos we observe around disk galaxies are made of metal-poor stars, or that they result from the integrated light of globular cluster populations. The correlation between the disk and halo SB suggests a link between the two components. On the other hand, the high latitude extension of the emission rules out ‘disk heating’ as an effective formation mechanism. An accretion (or ‘cannibalism’) scenario, in which the halo is built up by capture and disruption of spheroidal satellites, presents many advantages in explaining the observations. In this scenario dwarf spheroidal galaxies, made of old, metal enriched stars, are tidally disrupted by the gravitational field of the central galaxy and their stars are spread to fill the phase space almost isotropically in a few dynamical times. Thus both the spheroidal shapes and the extremely red colours of the halos could be explained, at least qualitatively. As already mentioned, recent observations in the halo of MW and M31, of the Sagittarius stream in the MW, and of the ring in the halo of NGC 5907 support the idea that this mechanism has been working till very recent times and is not uncommon among the disk galaxies.

Our analysis in different luminosity bins shows that the halo luminosity, at least on average, is proportional to disk luminosity. Prominent halos are in the more luminous galaxies. The decrease of the average surface brightness at lower luminosity affects mostly the redder pass-bands and is reflection of the well known correlation of disk surface brightness with disk luminosity in the red bands (see e.g.

---

\(^7\) Photometric transformations between different standards are taken from Smith et al. 2002.
The light we see does not appear to be a straightforward extension of the bulge, since the power-law shapes of the profiles, irrespective of luminosity, are not consistent with classical de Vaucouleurs or exponential bulges. We can interpret the halo-disc luminosity relation we find here in the hierarchical picture, in which more luminous galaxies sit in more massive DM halos, with a larger number of merging sub-halos contributing to the stellar halo luminosity. However, deeper and more detailed observations, along with more reliable theoretical predictions for the number, stellar mass and metal content of the accreted satellites, are needed in order to confirm this hypothesis.

6 SUMMARY AND CONCLUSIONS

By stacking a large number (> 1000) of edge-on disk galaxies imaged in the SDSS we have been able to detect a diffuse, spheroidal, low-surface brightness component around the disk. This detection is significant in the $g$, $r$, $i$ and $z$ bands, and cannot be ascribed to any obvious instrumental artifact (e.g. scattered light or PSF). Given the statistical estimator we adopt for combining the images, our result indicates that a substantial fraction of the stacked galaxies must share the observed halo characteristics, even if we cannot exclude the possibility that a number of disk galaxies actually have no halo at all. The halo can be described by a power-law projected density profile $I \propto r^{-\alpha}$, with $\alpha \sim 2$ nearly irrespective of the band.

The colour measurements provide inconclusive and troublesome results, but there is a clear indication for extremely red colours. $g - r$ is consistent with old, moderately metal-poor stellar populations, such as the more metal-rich MW’s globular clusters, 47 Tucanae, the halo of M31 and the most metal-poor stellar populations, such as the more metal-rich MW’s with $\alpha_i$ and red colours.

The colour measurements provide inconclusive and troublesome results, but there is a clear indication for extremely red colours. $g - r$ is consistent with old, moderately metal-poor stellar populations, such as the more metal-rich MW’s globular clusters, 47 Tucanae, the halo of M31 and the most metal-poor ellipticals. $r - i$ is (at 2 $\sigma$) 0.2 mag redder than the reddest known stellar populations in globular clusters and elliptical galaxies and it is difficult to reconcile with any theoretical models, even allowing for ad hoc modified IMF’s dominated by low-mass stars and high metallicity. The colour measurements provide inconclusive and troublesome results, but there is a clear indication for extremely red colours. $g - r$ is consistent with old, moderately metal-poor stellar populations, such as the more metal-rich MW’s globular clusters, 47 Tucanae, the halo of M31 and the most metal-poor ellipticals. $r - i$ is (at 2 $\sigma$) 0.2 mag redder than the reddest known stellar populations in globular clusters and elliptical galaxies and it is difficult to reconcile with any theoretical models, even allowing for ad hoc modified IMF’s dominated by low-mass stars and high metallicity. The data also suggest a correlation between the luminosity of the halo and the total luminosity of the galaxy.

The results presented in this work are far from being conclusive, but nevertheless they are consistent with the idea that a large fraction of disk galaxies are surrounded by a luminous halo. The colours, although affected by large uncertainties, hint at old, but not particularly metal-poor stellar populations, thus supporting a scenario in which the halos are mostly contributed by stars stripped from accreted or merged companions, in which the chemical evolution was already advanced.

Deeper, individual observations of a large sample of nearby galaxies will be required, however, in order to assess the validity of this scenario by quantifying not only the average halo, but also the whole distribution of individual halo parameters.

We wish to thank the referees James Lequeux and Françoise Combes for helpful advice.

S.Z. wishes to thank Annette Ferguson, Stéphane Charlot, Amina Helmi and Tim McKay for the useful discussions.

Funding for the creation and distribution of the SDSS Archive has been provided by the Alfred P. Sloan Foundation, the Participating Institutions, the National Aeronautics and Space Administration, the National Science Foundation, the U.S. Department of Energy, the Japanese Monbukagakusho, and the Max Planck Society. The SDSS Web site is http://www.sdss.org/

The SDSS is managed by the Astrophysical Research Consortium (ARC) for the Participating Institutions. The Participating Institutions are The University of Chicago, Fermilab, the Institute for Advanced Study, the Japan Participation Group, The Johns Hopkins University, Los Alamos National Laboratory, the Max-Planck-Institute for Astronomy (MPIA), the Max-Planck-Institute for Astrophysics (MPA), New Mexico State University, University of Pittsburgh, Princeton University, the United States Naval Observatory, and the University of Washington.

REFERENCES

Abazajian K., et al. 2003, preprint(astro-ph/0305492)
Abe F., et al. 1999, AJ, 118, 261
Barnaby D., Thronson H. A., 1994, AJ, 107, 1717
Baugh C. M., Cole S., Frenk C. S., 1996, MNRAS, 283, 1361
Benson A. J., Baugh C. M., Cole S., Frenk C. S., Lacey C. G., 2000, MNRAS, 316, 107
Bernardi M., et al. 2003, AJ, 125, 1882
Bertin E., Arnouts S., 1996, A&AS, 117, 393
Binney J., Merrifield M., 1998, Galactic astronomy. Princeton University Press, Princeton, NJ
Blanton M. R., et al. 2002, preprint(astro-ph/0210215)
Blanton M. R., Lin H., Lupton R. H., Maley F. M., Young N., Zehavi I., Loveday J., 2003, AJ, 125, 2276
Dalcanton J. J., Bernstein R. A., 2002, AJ, 124, 1328
Elson R. A. W., Fall S. M., Freeman K. C., 1987, ApJ, 323, 54
Ferguson A. M. N., Irwin M. J., Ibata R. A., Lewis G. F., Tanvir N. R., 2002, AJ, 124, 1452
Fry A. M., Morrison H. L., Harding P., Boroson T. A., 1999, AJ, 118, 1209
Fukugita M., Ichikawa T., Gunn J. E., Doi M., Shimasaku K., Schneider D. P., 1996, AJ, 111, 1748
Gavazzi G., Boselli A., Donati A., Franzetti P., Scodellino M., 2003, A&A, 400, 451
Gunn J. E., et al. 1998, AJ, 116, 3040
Harris W. E., 1976, AJ, 81, 1095
Harris W. E., 1996, AJ, 112, 1487
Hartwick F. D. A., 1987, in NATO ASIC Proc. 207: The Galaxy The structure of the Galactic halo. pp 281–290
Helmi A., White S. D. M., de Zeeuw P. T., Zhao H., 1999, Nature, 402, 53
Hogg D. W., Finkbeiner D. P., Schlegel D. J., Gunn J. E., 2001, AJ, 122, 2129
Ibata R. A., Gilmore G., Irwin M. J., 1994, Nature, 370, 194
Ibata R. A., Irwin M. J., Lewis G. F., Ferguson A. M. N., Tanvir N., 2003, MNRAS, 340, L21
Halos around edge-on disk galaxies in the SDSS

Ivezić Z., et al. 2000, AJ, 120, 963
James P. A., Casali M. M., 1998, MNRAS, 301, 280
Kauffmann G., Colberg J. M., Diaferio A., White S. D. M., 1999, MNRAS, 303, 188
Kauffmann G., Nusser A., Steinmetz M., 1997, MNRAS, 286, 795
Kauffmann G., White S. D. M., Guiderdoni B., 1993, MNRAS, 264, 201
Kinman T. D., Suntzeff N. B., Kraft R. P., 1994, AJ, 108, 1722
Kregel M., van der Kruit P. C., de Grijs R., 2002, MNRAS, 334, 646
Lequeux J., Combes F., Danetl-Fort M., Cuillandre J.-!C., Fort B., Mellier Y., 1998, A&A, 334, L9
Lequeux J., Fort B., Danetl-Fort M., Cuillandre J.-!C., Mellier Y., 1996, A&A, 312, L1
Lupton R. H., Gunn J. E., Ivezić Z., Knapp G. R., Kent S., Yasuda N., 2001, in ASP Conf. Ser. 238: Astronomical Data Analysis Software and Systems X The SDSS Imaging Pipelines. pp 269–
MacArthur L. A., Courteau S., Holtzman J. A., 2003, ApJ, 582, 689
Majewski S. R., 1993, ARA&A, 31, 575
Morrison H. L., Miller E. D., Harding P., Stinebrinig D. R., Boroson T. A., 1997, AJ, 113, 2061
Navarro J. F., Steinmetz M., 2000, ApJ, 538, 477
Navarro J. F., White S. D. M., 1994, MNRAS, 267, 401
Odenkirchen M., Grebel E. K., Dehnen W., Rix H., Cudworth K. M., 2002, AJ, 124, 1497
Petrosian V., 1976, ApJ, 209, L1
Pier J. R., Munn J. A., Hindsley R. B., Hennessy G. S., Kent S. M., Lupton R. H., Ivezić Z., 2003, AJ, 125, 1559
Preston G. W., Shectman S. A., Beers T. C., 1991, ApJ, 375, 121
Pritchet C. J., van den Bergh S., 1994, AJ, 107, 1730
Racine R., 1991, AJ, 101, 865
Rauscher B. J., Lloyd J. P., Barnaby D., Harper D. A., Hereld M., Loewenstein R. F., Severson S. A., Mrozek F., 1998, ApJ, 506, 116
Rudy R. J., Woodward C. E., Hodge T., Fairfield S. W., Harker D. E., 1997, Nature, 387, 159
Sackett P. D., Morrison H. L., Harding P., Boroson T. A., 1994, Nature, 370, 441
Saha A., 1985, ApJ, 289, 310
Scannapieco C., Tissera P. B., 2003, MNRAS, 338, 880
Schlegel D. J., Finkbeiner D. P., Davis M., 1998, ApJ, 500, 525
Shen S., Mo H. J., White S. D. M., Blanton M. R., Kauffmann G., Voges W., Brinkmann J., Csabai I., 2003, preprint (astro-ph/0301527)
Smith J. A., et al. 2002, AJ, 123, 2121
Sommer-Larsen J., Gelato S., Vedel H., 1999, ApJ, 519, 501
Somerville R. S., Primack J. R., 1999, MNRAS, 310, 1087
Springel V., White S. D. M., Tormen G., Kauffmann G., 2001, MNRAS, 328, 726
Stoughton C., et al. 2002, AJ, 123, 485
Strauss M. A., et al. 2002, AJ, 124, 1810
van der Kruit P. C., 2001, in ASP Conf. Ser. 230: Galaxy Disks and Disk Galaxies Truncations in Stellar Disks. pp 119–126
Wu H., et al. 2002, AJ, 123, 1364
Yanny B., Newberg H. J., Grebel E. K., Kent S.,