Spiral arms in thermally stratified protoplanetary discs

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ABSTRACT

Spiral arms have been observed in nearly a dozen protoplanetary discs in near-infrared scattered light and recently also in the sub-millimetre continuum. While one of the most compelling explanations is that they are driven by planetary or stellar companions, in all but one cases such companions have not yet been detected and there is even ambiguity on whether the planet should be located inside or outside the spirals. Here we use 3D hydrodynamic simulations to study the morphology of spiral density waves launched by embedded planets taking into account the vertical temperature gradient, a natural consequence of stellar irradiation. Our simulations show that the pitch angle of the spirals in thermally stratified discs is the lowest in the disc mid-plane and increases towards the disc surface. We combine the hydrodynamic simulations with 3D radiative transfer calculations to predict that the pitch-angle of planetary spirals observed in the near-infrared is higher than in the sub-millimetre. We also find that in both cases the spirals converge towards the planet. This provides a new powerful observational method to determine if the perturbing planet is inside our outside the spirals, as well as map the thermal stratification of the disc.

Key words: accretion, accretion discs — circumstellar matter — protoplanetary discs — hydrodynamics

1 INTRODUCTION

With the dawn of extreme high resolution imaging capabilities of current telescopes (e.g. SPHERE/VLT, GPI/Gemini, ALMA) more and more discs show spiral arms in near-infrared (NIR) scattered light (e.g. Muto et al. 2012; Benisty et al. 2015; Wagner et al. 2015; Stolker et al. 2016; Benisty et al. 2017) and recently also in the sub-millimetre (Pérez et al. 2016; Tobin et al. 2016). The observed spirals have similar morphologies in most cases; two symmetric arms, shifted in azimuth by approximately 180°, and with a pitch angle of about 15°–30°. In most cases there is also a gap / cavity just inwards of the spirals.

It has been known for a long time that spiral density waves are launched by planetary or stellar companions at Lindblad-resonances (e.g., Goldreich & Tremaine 1979; Ogilvie & Lubow 2002; Rafikov 2002) both inwards and outwards of the companion’s orbit. Therefore a straightforward explanation for the observed spirals is that they are launched by so far undetected companion (possibly a forming, embedded planet), (e.g. Muto et al. 2012; Grady et al. 2013); this would open up the exciting possibility of getting a direct insight into planet formation. Using 2D hydrodynamic simulations and 3D radiative transfer computation Juhász et al. (2015) showed, however, that the pitch angle and contrast of the spirals driven by planets orbiting inwards of the spirals are not compatible with the NIR observations. Dong et al. (2015a) combined 3D hydrodynamic simulation with 3D radiative transfer calculations to show that the observed contrast and pitch angle of spirals are in fact in agreement with the spirals being launched by massive (several M_Jup) planets exterior to the spirals.

However, planets are not the only explanations for the observed spirals. Multi-armed spiral structure can also form due to gravitational instability (GI, see e.g. Rice et al. 2003) with the number of arms depending on the mass and temperature of the disc via the Toomre $Q$ parameter (Cossins et al. 2009). For very massive discs ($M_\text{disc}/M_\star \gtrsim 0.25$), GI can produce two armed spirals in the disc, similar to the NIR scattered light observations (Dong et al. 2015b). Meru et al. (2017) showed that GI could explain the spirals in the sub-millimetre ALMA images of Elias 2–27.

Additionally, if a marginally gravitationally stable disc is perturbed by an embedded planet, the tidal interaction might tip the balance and trigger GI in the disc (Polgl et al. 2015). This combined mechanism may also produce spirals with pitch angles similar to the ones in observations.

Numerous theoretical studies have recently increased the level of complexity in the modelling of spirals, show-
ing the importance to understand their origin. For instance, while tidally induced spiral density waves have been studied for a long time in 2D, Zhu et al. (2015) demonstrated the spiral amplitude and pitch angle (the complement of the angle between radial direction and the tangent of the spiral) in the non-linear regime are higher in 3D than in 2D simulations. However, an important aspect of a realistic disc model has not yet been investigated. Protoplanetary discs in which spirals have been detected are passively heated by the absorbed stellar radiation. As a consequence of this they will have a positive vertical temperature gradient (Chiang & Goldreich 1997), resulting in a vertical thermal stratification in the disc. It is known that the pitch angle of the spirals depends on the local sound speed (Rafikov 2002), thus we expect vertical thermal stratification to affect the morphology of the spiral wake. The goal of this study is to investigate the morphology of tidally induced spirals by embedded planets in 3D thermally stratified discs. We note, however, that our results would also be applicable to stellar companions as the tidal interaction between the disc and the companion is the same as for the planetary case.

2 MODELING

2.1 Hydrodynamic simulations

We run 3D hydrodynamical simulations with the code PLUTO (Mignone et al. 2007) to investigate the disc response to the planet. We include the FARGO algorithm (Mignone et al. 2012) to reduce the computational cost and use the HLLC Riemann solver, linear reconstruction and second order Runge-Kutta time integration. We employ a spherical grid with 400, 500 and 1024 cells, distributed in the [0.4, 2.5], [1.22, $\pi/2$], and [0, 2$\pi$], intervals in the radial, polar and azimuthal directions. The planet was placed at the coordinates [1.0, 0, $\pi/4$]. In the radial and polar directions we define “wave-killing zones” where we damp disturbances, following de Val-Borro et al. (2006), extending up to 0.44 and from 2.25 in radius and until 1.27 in $\theta$. We employ a locally isothermal equation of state, in which the sound speed $c_s$ is a function of position only, and a physical viscosity using the Shakura & Sunyaev (1973) prescription with a value of $\alpha = 10^{-3}$. We assume the planet mass to be $3M_{\text{Jup}}$.

We run two simulations, the first (subsequently called “isothermal”) in which $c_s$ depends only on radius: $c_s \propto r^{-1/4}$, with the normalization set such that the disc aspect ratio at the location of the planet is 0.07, a typical value at tens of AU. In the second simulation (“stratified”), we allow the sound speed to vary as a function of the vertical coordinate. To this end we use the prescription commonly employed when fitting observations of Dartois et al. (2003) and subsequently updated by Rosenfeld et al. (2013). We assume that the temperature in the upper layer of the disc is 2.5 times the value in the midplane (the same as in the isothermal case), and that the transition between the cold mid-plane and the hot upper layer (the parameter $z_\theta$ of Dartois et al. 2003) happens at 3 scale-heights. The initial surface density $\Sigma$ of the disc follows $\Sigma \propto r^{-3}$. We solve for the hydrostatic equilibrium in the vertical direction to assign the initial density at every point and we initialise the velocity so that the gas is initially in Keplerian rotation. We evolve the simulations for 100 orbits to reach a steady state in the structure of the spirals.

2.2 Radiative transfer simulations

We calculate images from the hydrodynamical simulations using the 3D radiative transfer code radmc-3d\(^1\), using the same 3D spherical mesh of the hydrodynamical simulations. We assume that the central star is a Herbig Ae star ($T_{\text{eff}}=9500$ K, $M_*=2.5M_\odot$, $R_*=2.0R_\odot$), a constant gas-to-dust ratio of 100 and we calculate the dust opacity assuming astronomical silicate (Weingartner & Draine 2001) for a grain size distribution of $n(a) \propto a^{-3.5}$ between $a = 0.1\mu$m and $a = 1\mm$. With radmc-3D we first calculate the dust temperature with a thermal Monte-Carlo simulation and we then calculate images at wavelengths $\lambda = 1.65\mu$m and $\lambda = 1.3\mm$ and for an inclination of $0^\circ$. Finally we generate synthetic observations by convolving the calculated images with a Gaussian kernel with an FWHM of 0.04", typical of current state-of-the-art near-infrared cameras such as SPHERE/VLT or GP1/Gemini and of ALMA (ALMA Partnership et al. 2015). We assume a source distance of 100 pc.

3 RESULTS

3.1 Hydrodynamic simulations

We show in figure 1 the pitch angle of the spiral in the stratified simulation as a function of the height above the midplane. We plot with the colours shown in the legend the pitch angle at different radii; in addition the dependence of the pitch angle closely resembles the one of the sound speed. This behaviour is the natural consequence of the temperature dependence of the pitch angle. The spirals are located where constructive interference occurs between waves

\(^1\) http://www.ita.uni-heidelberg.de/~dullemond/software/radmc-3d/
emitted from Lindblad resonances in the disc (Ogilvie & Lubow 2002); this location depends on the wave propagation speed, and thus the disc temperature. Indeed Rafikov (2002) showed that the pitch angle of a tidally induced spiral in a 2D Keplerian disc, in which the sound speed varies with radius as $c_s = c_p(r/r_p)^{-q}$, depends on the sound speed:

$$\beta = \pi/2 - \tan^{-1} \left( \frac{r_p}{h_p} \left( \frac{r}{r_p} \right)^{q+1} \left( \frac{r_p}{r} \right)^{3/2} - 1 \right)$$  \hspace{1cm} (1)$$

where $\beta$ is the pitch angle, $r_p$ is the orbital radius of the planet and $h_p$ is the pressure scale height (which depends on the sound speed via $h_p = c_p/\Omega_p$). The resemblance between the dependence with the vertical coordinate of the pitch angle and the sound speed profile may imply that this relation holds also in a 3D disc, provided that the local temperature is used in the relation. We leave a detailed analysis of the pitch angle in 3D to further studies and conclude that the vertical temperature gradient increases the pitch angle of the spirals in the upper layers of the disc.

### 3.2 Simulated observations

We show the simulated NIR scattered light and sub-millimetre continuum images calculated from vertically isothermal (see Figure 2a,b) and thermally stratified (see Figure 2c,d) hydrodynamic simulations. In terms of the general structure, the isothermal and stratified simulation look largely similar, with the only significant difference that the inner part of the disc in the stratified simulation is brighter with respect to the isothermal simulation. This is because the inner edge of the disc in the stratified simulation is more "rounded off", increasing the flaring index of the disc locally and consequently the brightness of the disc.

#### 3.2.1 Amplitude of the spirals

In Figure 3 we compare the azimuthal surface brightness profiles of the two models at two radii, 1.7$r_p$ and 0.58$r_p$. From this plot we measure the peak-to-peak variation of the intensity in the azimuthal direction and the full width at half maximum of the spiral peak (for the inner spiral we considered the stronger, primary arm). Since the two models employ the same temperature in the disc midplane, in the sub-millimetre case (Figure 3b, d) the peak-to-peak intensity variation and the width of the spiral peak agree within
10%. In the near-infrared scattered light images (Figure 3a, c) instead the spiral contrast is higher in the isothermal simulations by 49% and 45% in the inner and outer arms, respectively. This is caused by the higher temperature in the upper layers in the stratified simulations; the enhanced pressure forces tend to wash out more the spiral wake and reduce its amplitude. While the azimuthal width of the spirals in the two simulations agree to 4% inwards of the planet, for the outer spirals in the isothermal models the azimuthal width is a factor of 3.5 times larger compared to the stratified simulations.

3.2.2 Spiral wake

In Figure 4 we present the spiral wakes we derived from the synthetic images by extracting the positions of the local maxima in the radial surface brightness distribution. In sub-millimetre images, probing the disc mid-plane, the spirals have similar pitch angles in the locally isothermal and in the vertically stratified simulations (see Figure 4a and Figure 4d) since the mid-plane temperatures in the two simulations (locally isothermal vs. stratified) are identical.

Spirals in scattered light images computed from stratified simulations (see Figure 4c) instead are more open compared to the ones computed from locally isothermal simulations (see Figure 4b), consistently with the analysis of the simulation in section 3.1. For example, while we find that outer spirals in NIR scattered light images have a low pitch angle (7.5° at 1.5r_pl) in the isothermal simulations, the pitch angle is higher in the stratified simulation (13° at 1.5r_pl); the effect is smaller for the inner spiral (15° vs 13° at 0.7r_pl). Dong et al. (2015a) suggested that a low pitch angle could be used to identify the spiral as an outer one, but it is not clear whether this method still applies to the stratified case.

To better illustrate the difference in opening angle we show the difference in azimuth angles between the spirals derived from scattered light and sub-millimetre images as a function of stellocentric radius in Figure 4c and Figure 4f for the locally isothermal and for the stratified simulations, respectively. In the locally isothermal simulation the difference in the azimuthal position of the spiral wake is not larger than 8° for the inner arms at all radii with a weak trend of increasing difference towards smaller radii. For the outer spirals the difference fluctuates between -19° and -6° with no clear dependence on the radius. In case of the stratified simulations there is a clear trend for the azimuthal position difference of the spirals in near-infrared and sub-millimetre. The azimuthal difference in the spiral position increases both inwards and outwards from the position of the planet. The difference in the spiral position in near-infrared and sub-millimetre images is nearly -20° for the inner arms at 0.55r_pl in the stratified simulations compared to the -8° in the locally isothermal simulations. For the outer arms the azimuthal position difference is about 30° at 2r_pl in the stratified simulations while only -15° in the locally isothermal simulations.

4 DISCUSSION AND CONCLUSIONS

Direct detection of young planets is notoriously difficult due to the contrast limitation of the observations. Due to their larger spatial extent, spiral density waves excited by young planets are easier to detect. Thus, spiral arms could, in principle, be used as signposts of planets (see e.g. Dong et al. 2015a). However, there is ambiguity in whether the planet is inside or outside the spirals. In the previous section we have shown that the spiral arms in the sub-mm and in scattered light converge towards the location of the planet due to the different temperature in the midplane compared to the upper layers of the disc. Therefore, we suggest to use the direction of convergence of the spirals in near-infrared...
and in sub-millimetre continuum images to infer whether the planet is inwards or outwards of the spirals.

Observationally, this requires having high-resolution observations of the same disc in near-infrared scattered light, probing the upper layers of the disc, and in sub-millimetre continuum, probing the disc mid-plane. Although not explored in this paper, we note that optically thin gas observations also trace the disc midplane and could therefore be used in place of the sub-mm continuum.

We also note that, if we know that a planet is responsible for the perturbation, the dependence of the spiral pitch angle on the local temperature could be used as a diagnostic to map the vertical thermal stratification of the disc. This method requires using different tracers (e.g. NIR scattered light, various CO isotopologues, sub-mm-continuum) coming from different heights above the midplane. Mapping the vertical thermal structure of the disc with the spiral pitch angle has the advantage over other alternative methods (e.g. modelling of the dust continuum emission, molecular rotational transitions), that the pitch angle depends only on the dynamics and is not affected by uncertainties in chemistry and opacities. While the absolute value of the pitch angle might be weakly affected by the planet mass or viscosity (Dong & Fung 2017), the differential variation of it as a function of height is likely independent of these factors. A detailed mapping will require a non-linear theory of spiral density waves in thermally stratified discs, which has yet to be developed.

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Figure 4. Panel a and b show the spiral wake in the vertically isothermal simulation inwards and outwards of the planetary orbit, respectively. Panel c shows the difference in the azimuthal position of the spirals between sub-mm and NIR scattered light images as a function of radius. Panel d–f are for the vertically stratified simulation. In a vertically isothermal disc the shape of the spiral wake is largely the same at both wavelengths. For the stratified simulation the spirals are more open in the NIR than in the sub-mm both inwards and outwards of the planetary orbit. In the stratified simulation the difference in the azimuthal position of the spirals between NIR and sub-millimetre increases with increasing distance from the planet, i.e. the spirals converge towards the planet.