Dynamic effects in double graphene-layer structures with inter-layer resonant-tunnelling negative conductivity

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Abstract
We study the dynamic effects in the double graphene-layer (GL) structures with the resonant-tunnelling (RT) and the negative differential inter-GL conductivity. Using the developed model, which accounts for the excitation of self-consistent oscillations of the electron and hole densities and the ac electric field between GLs (plasma oscillations), we calculate the admittance of the double-GL RT structures as a function of the signal frequency and applied voltages, and the spectrum and increment/decrement of plasma oscillations. Our results show that the electron–hole plasma in the double-GL RT structures with realistic parameters is stable with respect to the self-excitation of plasma oscillations and aperiodic perturbations. The stability of the electron–hole plasma at the bias voltages corresponding to the inter-GL RT and strong nonlinearity of the RT current–voltage characteristics enable using the double-GL RT structures for detection of terahertz (THz) radiation. The excitation of plasma oscillations by the incoming THz radiation can result in a sharp resonant dependence of detector responsivity on radiation frequency and the bias voltage. Due to a strong nonlinearity of the current–voltage characteristics of the double-GL structures at RT and the resonant excitation of plasma oscillations, the maximum responsivity, \(R_{\text{max}}\), can markedly exceed the values \((10^4–10^5)\) V W\(^{-1}\) at room temperature.

(Some figures may appear in colour only in the online journal)

1. Introduction
As demonstrated recently [1–4], double graphene-layer (GL) structures with the inter-GL layers forming relatively narrow and low energy barriers for electrons or holes can be effectively used in novel devices. The excitation of plasma oscillations in these structures, i.e., the excitation of spatio-temporal variations of the electron and hole densities in GLs and the spatio-temporal variations of the self-consistent electric field between GLs, by incoming terahertz (THz) radiation, modulated optical radiation, or ultra-short optical pulses provides additional functional opportunities. In particular, the double-GL structures with the inter-GL tunnelling or thermionic conductance can be used in the resonant THz detectors and photomixers [5, 6]. As was recently discussed [7–9] and realized experimentally [10], the inter-GL resonant tunnelling (RT) in the double-GL structures, with the band diagrams properly aligned by the applied voltage, leads to inter-GL negative differential conductivity (NDC) and enables novel transistor designs with the multi-valued current–voltage characteristics. A strong nonlinearity of the inter-GL current–voltage characteristics at the voltages near tunnelling resonance can be used in double-GL-based frequency multipliers [8], detectors [5], and other microwave and THz devices. However, NDC might, in principle, result in the instability of stationary states, modifying or even harming...
normal operation of double-GL transistors and two-terminal devices.

In this paper, we consider the double-GL structures with tunnelling transparent barrier layers exhibiting RT and NDC. Using the proposed model, we calculate the device admittance and demonstrate that a steady-state current flow in these structures is stable with respect to the self-excitation of plasma oscillations and aperiodic perturbations despite NDC. The incoming electromagnetic radiation, particularly, THz radiation can result in an effective resonant excitation of plasma oscillations, which can be used for the THz detection. We calculate the rectified current and the responsivity of the THz detectors based on the double-GL RT structures and show, that due to a strong nonlinearity of the double-GL current–voltage characteristics and the possibility of the resonant excitation of plasma oscillations by incoming THz radiation, the structures under consideration can serve as THz detectors exhibiting very high responsivity.

2. Model equations

We consider the double-GL structures either with chemically doped GLs (figure 1(a)) or with undoped GLs but sandwiched between two highly conducting gates (figure 1(b)). In the first case, one of the GLs is doped by donors, whereas the other one is doped by acceptors, so that the electron and hole sheet densities in the pertinent GLs are approximately equal to the dopant density (donors and acceptors) $\Sigma_1$. In the second case, the voltage $V_g$ applied between the gates, induces the electrons and holes with the sheet charge densities $\pm e \Sigma_1 \propto V_g/W_g$, where $W_g$ is the thickness of the layers separating GLs and the gates (see figure 1(b)).

Each GL is supplied by an ohmic side contact (left-side contact to lower GL and right-side contact to upper GL) between which the bias voltage $V_b$ is applied. This voltage affects the electron and hole steady-state densities $\Sigma_0$:

$$\Sigma_0 = \Sigma_1 + \frac{\kappa \Delta_0}{4\pi e^2 d}. \tag{1}$$

Here $e = |e|$ is the value of the electron charge, $\kappa$ is the dielectric constant, and $d$ is the spacing between GL (i.e. the thickness of the inter-GL barrier). The steady-state value of the energy difference, $\Delta_0$, between the Dirac points in GLs is determined by the following equation:

$$\Delta_0 = 2\varepsilon_F - eV_0. \tag{2}$$

where $\varepsilon_F$ is the Fermi energy of electrons and holes in the pertinent GL. Equations (1) and (2) account for the effect of quantum capacitance [11]. Figures 1(c) and (d) show the band diagrams of the double-GL structures under consideration at $V_0 < V_t$ and $V_0 = V_t$, respectively. In practically interesting cases, the electron and hole systems in GLs are degenerated even at room temperatures. This occurs when $\Sigma_1$ is sufficiently large in comparison with the equilibrium density $\Sigma_T$: $\Sigma_1 \gg \Sigma_T = \frac{\hbar k_{\text{B}} T^2}{6\pi^2 \varepsilon_0^2}$, where $\hbar$ and $k_{\text{B}}$ are the Planck and Boltzmann constants, respectively, $\varepsilon_0 \approx 10^8 \text{ cm}^{-1}$ is the characteristic velocity of electrons and holes in GLs, and $T$ is the temperature. In such a case,

$$\varepsilon_F = \hbar v_W \sqrt{\pi \left( \Sigma_1 + \frac{\kappa \Delta_0}{4\pi e^2 d} \right)}. \tag{3}$$

Using equations (1) and (2) and the alignment condition $\Delta = 0$, we obtain the following formula for the alignment voltage:

$$V_t = 2\varepsilon_F/e = 2\hbar v_W / \pi \Sigma_1/e. \tag{4}$$

The local value of the inter-GL RT current density as a function of the local value of the inter-GL voltage $V$ is given by [7, 8]

$$j_t = j_t^{\text{max}} \exp \left[ -\frac{V - V_t}{\Delta V_t} \right]. \tag{5}$$

where $j_t^{\text{max}}$ is the peak value of the current density and $\Delta V_t \approx 2\sqrt{2}\pi e \hbar v_W / \epsilon_l$ determines the peak width, $l$ is the coherence length (the characteristic size of the ordered areas in GLs).

Using equation (5), at small signal variations of the local potential difference between GLs ($\delta \varphi_2 - \delta \varphi_1$), the variation of the RT current density can be presented as

$$\delta j_t \simeq \sigma_t (\delta \varphi_2 - \delta \varphi_1) + \beta_t (\delta \varphi_1 - \delta \varphi_2)^2. \tag{6}$$

Here $\sigma_t = (d j_t/dV)|_{V=V_t}$ is the differential tunnelling conductivity and $\beta_t = \frac{1}{2} (d^2 j_t/dV^2)|_{V=V_t}$ determines the nonlinearity of the RT current–voltage characteristics:

$$\sigma_t = -\frac{2j_t^{\text{max}}}{\Delta V_t^2} \left( \frac{V_0 - V_t}{\Delta V_t} \right) \exp \left[ -\left( \frac{V_0 - V_t}{\Delta V_t} \right)^2 \right]. \tag{7}$$

$$\beta_t = \frac{2j_t^{\text{max}}}{\Delta V_t^3} \left( 2 \left( \frac{V_0 - V_t}{\Delta V_t} \right)^2 - 1 \right) \exp \left[ -\left( \frac{V_0 - V_t}{\Delta V_t} \right)^2 \right]. \tag{8}$$

As follows from equation (7), $\sigma_t$ changes its sign at $V_0 = V_t$ and becomes negative when $V_0 > V_t$. The maximum value

\[ Figure 1. Schematic views of (a) a doped double-GL structure and (b) a gated double-GL structure with ‘electrical’ doping. (c) band diagram at $V_0 < V_t$ and (d) at $V_0 = V_t$. Horizontal arrows correspond to inter-GL non-resonant and RT transitions. \]
of \(|\sigma_v|\), which is achieved at \(V_0 = V_i = \pm \Delta V_i / \sqrt{2}\), is equal to \(|\sigma_v| = \sqrt{2}e^{-1/2}(j_{i,\max} / \Delta V_i)\). Equation (8) for the value \(\rho_i\) at \(V_0 = V_i\) yields \(\beta = -2j_{i,\max} / (\Delta V_i)^2\). For brevity, in the following we omit a relatively small value \((\hbar \frac{vW_1}{\sqrt{2e}} / 8e^2\varepsilon_F d)\), which is ratio of the geometrical capacitance \(C = \kappa / 4\pi d\) and the quantum capacitance \(C_0 = 2e^2 e_F / \pi \hbar^2 e_F^2\).

The spatial distributions of \(\delta \varphi_\pm(x)\) and \(\delta \varphi_- (x)\) in the GL plane (along the axis \(x\)) can be found from linearized hydrodynamic equations (adopted for the energy spectra of the electrons and holes in GLs [12]) coupled with the Poisson equation in the gradual channel approximation [13]. We limit our treatment to the in-phase perturbations of the electron and hole densities. For such perturbations, the self-consistent ac electric field is located between GLs. The difference in the local values of the ac potentials of the upper and lower GLs causes the inter-GL current, which can either increase or decrease with varying \((\delta \varphi_\pm - \delta \varphi_-)\) depending on the value of \(V_0 - V_i\). For the out-of-phase perturbations of the electron and hole densities, the ac electric field is located mainly outside the double-GL structure, so that the inter-GL tunnelling is insignificant and no effects associated with NDC can be expected.

Calculating the ac potentials, one can neglect the nonlinear component of the ac inter-GL current, i.e., the second term in equation (6) (see, however, section 4) and searching for the ac potential in the following form:

\[ \delta \varphi_{\pm} = \delta \varphi_{\pm}(x) \exp(-i\omega t), \]

where \(\omega\) is the complex signal frequency. In this case, the system of equations in question can be reduced to the equations for the ac components of the potential at the frequency \(\omega\) [3, 4]:

\[
\frac{d^2 \delta \varphi_{\pm}}{dx^2} + \frac{\omega (\omega + iv) }{s^2} (\delta \varphi_{\pm} - \delta \varphi_-) = -i\delta j (\omega + iv) \frac{4\pi d}{\kappa s^2}, \tag{9}
\]

\[
\frac{d^2 \delta \varphi_-}{dx^2} + \frac{\omega (\omega + iv) }{s^2} (\delta \varphi_- - \delta \varphi_{\pm}) = i\delta j (\omega + iv) \frac{4\pi d}{\kappa s^2}. \tag{10}
\]

Here \(v\) is the collision frequency of electrons and holes in GLs with impurities and acoustic phonons and \(s\) is the characteristic velocity of plasma waves in double-GL structures. Since electrons and holes belong to different GLs separated by a relatively high barrier, we have disregarded the electron-hole scattering and, hence, the effect of mutual electron-hole drag [12]. The characteristic velocity \(s\) in the double-GL structures (similar to that in the two-dimensional electron or hole channels in the standard semiconductors with metal gates) is determined by the net dc electron and hole densities \(\Sigma_0\) and the inter-GL layer thickness \(d\) [14–17]. In double-GL structures with the degenerate electron–hole plasma, \(s = \sqrt{4\pi e^2 \Sigma_0 d / k m}\), where \(m \propto \sqrt{\Sigma_0}\) is the ‘fictitious’ mass of electrons and holes in GLs. This implies that \(s \propto \Sigma_0^{1/4}\) [14]. The value of \(s\) in the GL structures under consideration can be fairly high, always exceeding the characteristic velocity of electrons and holes in GLs \(vW_1\) [14, 18]. Considering equations (6), (9) and (10), we obtain

\[
\frac{d^2 \delta \varphi_-}{dx^2} + \frac{\omega (\omega + iv) (\omega + iv) }{s^2} (\delta \varphi_- - \delta \varphi_{\pm}) = 0. \tag{11}
\]

Here \(\gamma_i = 4\pi \sigma_i d / k\) is the characteristic frequency of the inter-GL tunnelling. At \(V_0 = V_i\), \(\sigma_i = 0\) and \(v_i = 0\), while at \(V_0 \gtrsim V_i\), \(\sigma_i < 0\) and, hence, \(v_i < 0\).

Assuming that the total voltage between the contacts to GLs is equal to \(V = V_0 + \delta V_{\omega}\), where \(\delta V_{\omega}\) is the small signal-voltage component, one can use the following boundary conditions for equations (11) and (12):

\[
\delta \varphi_{\pm}|_{x = \pm L} = \pm \delta V_{\omega} / 2 \exp(-i\omega t), \quad \frac{d \delta \varphi_{\pm}}{dx} \bigg|_{x = \pm L} = 0. \tag{13}
\]

The latter boundary conditions reflect the fact that the electron and hole currents are equal to zero at the disconnected edges of GLs (at \(x = -L\) in the upper GL and at \(x = L\) in the lower GL), while the difference of the ac potentials \(\delta V_{\omega}\) can generally be nonzero.

Solving equations (11) and (12) with boundary conditions (13), we obtain

\[
\delta \varphi_{\pm} - \delta \varphi_- = \delta V_{\omega} \left( \frac{\cos \gamma_{\omega} x}{\cos \gamma_{\omega} L} \right) \left( \frac{\gamma_{\omega} \Sigma_0}{\gamma_{\omega} \Sigma_0} \right), \tag{14}
\]

where \(\gamma_{\omega} = \sqrt{2(\omega + iv) / s}\).

3. Admittance of the double-GL RT structures

First, we calculate the small-signal admittance of the double-GL RT structures, \(Y_{\omega} = \delta J_\omega / \delta V_{\omega}\), where

\[
\delta J_\omega = H \left( -i \frac{k}{4\pi d} + \sigma_1 \right) \int_{-L}^L dx (\delta \varphi_- - \delta \varphi_{\pm}) \tag{15}
\]

is the net ac current, including the displacement current and \(H\) is the width of the double-GL structure in the direction perpendicular to the currents. Using equations (14) and (15), we find

\[
Y_{\omega} = -i \left( \frac{k H L}{2\pi d} \right) \left( \frac{\omega + iv}{\omega + iv} \right) \frac{\gamma_{\omega} \Sigma_0}{\gamma_{\omega} \Sigma_0} \left( \frac{\omega + iv}{\omega + iv} \right) \tag{16}
\]

Here we have introduced the plasma frequency \(\Omega = (\pi \sqrt{2} L)\), so that \(\gamma_{\omega} L = \pi \sqrt{(\omega + iv)(\omega + iv) / \Omega}\). In the limit \(\omega \ll 0\), equation (16) yields \(Y_{\omega} = 2HL\sigma_1 / \Omega\), which implies that in this case the dc admittance is determined by the inter-GL conductivity. When \(\Omega^2 \ll (|v_1| v)\), we find \(Y_{\omega} = (2HL / 4\pi d) (\Omega / \pi v) \approx \sigma_0\), where \(\sigma_0 \propto (e^2 \Sigma_0 / mv)\) stands for the dc conductivity of GLs.

Figure 2 shows the frequency dependences of the real and imaginary parts of the admittance calculated using equation (16) for different values of the plasma oscillation quality factor \(Q = \Omega / (2\pi v)\) and \(\sigma_0 = 0.01\). As seen, \(\Re Y_{\omega}\) is negative in a narrow range of small frequencies. This is due to NDC at \((V_0 - V_T) \gtrsim \Delta V_i\) associated with RT. However, at higher signal frequencies, \(\Re Y_{\omega}\) is positive. One can also see that \(\Im Y_{\omega}\) does not change its sign in the frequency region, where \(\Re Y_{\omega} < 0\).
oscillation quality factor $Q$ is frequency $\omega/\Omega_1$ the frequency dependences in the range of low signal frequencies.

Admittance versus signal frequency $\omega/\Omega_1$ characteristic plasma frequency state of the electron–hole plasma at given bias voltage for the chosen parameters. Indeed, the stability of stationary yields $\omega = \nu - \nu_t$ for double-GL RT structures with different plasma oscillation quality factor $Q = \Omega/\nu > 1$ or $\nu_t < \Omega^2/\pi^2 \nu$ in the structures with $Q \ll 1$. In the former case, plasma oscillations with the frequencies $\omega_n$ can self-excite, while in latter case, the growth of the perturbations of the electron and hole densities is aperiodic, which could potentially result in the domain formation. In such situations, the stationary current flow between GLs could be unstable. However, in real double-GL structures the value of the differential inter-GL RT conductivity is not sufficiently large to provide the condition $\nu_t < -\nu$. To estimate the real value of $\nu_t$, we assume that $j_{\text{max}}^\nu \approx (5–30) \text{ A cm}^{-2} [8–10]$ and $l = 100 \text{ nm},$ so that $V_t \approx 30 \text{ mV}$. This yields $|\sigma| = (143–858) \text{ S cm}^{-2}$. If $d = 4 \text{ nm}$ and $\kappa = 4$ (hBN four atomic layers thick barrier), one obtains $|\nu_t| \approx (1.6–9.7) \times 10^8 \text{ s}^{-1}.$ As seen, at realistic $\nu = (10^{13}–10^{15}) \text{ s}^{-1},$ the value $|\nu_t| \ll \nu$. This is in contrast to the double-barrier RT devices based on InGaAs–AlAs, where the frequency $|\nu_t|$ can be rather high, being of the order of or even exceeding the electron collision frequency. This is due to a very high peak current density and modest width of the tunnelling resonance $\Delta V_t$ in the double-barrier RT diodes. This can lead to the instability of the stationary current with respect to the self-excitation of plasma oscillations [19]. For instance, in one of the best RT diode [20], $\kappa = 12, |\sigma| = 3.3 \times 10^6 \text{ S cm}^{-2}$ and $d = 31 \text{ nm},$ so that $V_t \approx 10^{13} \text{ s}^{-1}$.

In relatively long double-GL structures, inequality $\nu_t < -\Omega^2/\pi^2 \nu$ can be satisfied if the collision frequency $\nu$ is large and, hence, the mobility of electrons and holes is low. Indeed, setting $\Omega/2\pi \approx 0.14–0.28 \text{ THz}$ and $\nu = (1–5) \times 10^{13} \text{ s}^{-1},$ the latter inequality needs $|\nu_t| > (1.6–7.8) \times 10^8 \text{ s}^{-1}.$ The latter condition is not met for the double-GL structures considered recently [8–10].

4. Resonant detection of radiation

The ac potential $\delta V_\omega$ between the contacts to GLs can arise due incoming electromagnetic radiation received by an antenna. This results in the excitation of plasma oscillations in the double-GL structure described by equation (14). The ac potential drop $\delta \varphi_+ - \delta \varphi_-$ causes not only the linear component of the tunnelling current $\delta J_{\text{tunnel}}$ but also the rectified dc current, $\delta J_0$, associated with the nonlinear (quadratic) component. The rectified ac current is given by the following formula:

$$\delta J_0 = H \int_{-L}^{L} dx \beta_j |\delta \varphi_+ - \delta \varphi_-|^2,$$

If $\Omega \ll \nu$, we find $\omega' = 0$ from equation (17)

$$\Gamma = \frac{-\Omega^2}{\pi^2 \nu} - \nu_t.$$  

The plasma frequency can vary in a wide range depending on the structure length $2L$. In particular, setting $s = (2–4) \times 10^3 \text{ cm s}^{-1}$ and $2L = 1 \mu \text{m}$ (as in [10]), one obtains $\Omega/2\pi \approx 1.4–2.8 \text{ THz}$ (so that according to equation (18) $\omega_0 \approx 0.554–1.1 \text{ THz}$). But if $2L = 10 \mu \text{m}$, one can get $\Omega/2\pi \approx 0.14–0.28 \text{ THz}$.

As follows from equations (18) and (19), the plasma instability (the increment, i.e., the growth rate $\Gamma > 0$) is possible if $\nu_t < -\nu$ in the structures with a high quality factor $Q = \Omega/\nu > 1$ or $\nu_t < -\Omega^2/\pi^2 \nu$ in the structures with $Q \ll 1$. In the former case, plasma oscillations with the frequencies $\omega_n$ can self-excite, while in latter case, the growth of the perturbations of the electron and hole densities is aperiodic, which could potentially result in the domain formation. In such situations, the stationary current flow between GLs could be unstable. However, in real double-GL structures the value of the differential inter-GL RT conductivity is not sufficiently large to provide the condition $\nu_t < -\nu$. To estimate the real value of $\nu_t$, we assume that $j_{\text{max}}^\nu = (5–30) \text{ A cm}^{-2} [8–10]$ and $l = 100 \text{ nm},$ so that $V_t \approx 30 \text{ mV}$. This yields $|\sigma| = (143–858) \text{ S cm}^{-2}$. If $d = 4 \text{ nm}$ and $\kappa = 4$ (hBN four atomic layers thick barrier), one obtains $|\nu_t| \approx (1.6–9.7) \times 10^8 \text{ s}^{-1}.$ As seen, at realistic $\nu = (10^{13}–10^{15}) \text{ s}^{-1},$ the value $|\nu_t| \ll \nu$. This is in contrast to the double-barrier RT devices based on InGaAs–AlAs, where the frequency $|\nu_t|$ can be rather high, being of the order of or even exceeding the electron collision frequency. This is due to a very high peak current density and modest width of the tunnelling resonance $\Delta V_t$ in the double-barrier RT diodes. This can lead to the instability of the stationary current with respect to the self-excitation of plasma oscillations [19]. For instance, in one of the best RT diode [20], $\kappa = 12, |\sigma| = 3.3 \times 10^6 \text{ S cm}^{-2}$ and $d = 31 \text{ nm},$ so that $V_t \approx 10^{13} \text{ s}^{-1}$.

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$$\delta J_0 = H \int_{-L}^{L} dx \beta_j |\delta \varphi_+ - \delta \varphi_-|^2,$$
This rectified component of the inter-GL RT current can be used for detection of THz signals. Using equations (14) and (20), we obtain the following formulae for the rectified current $\delta I_0$ and the detector volt–watt responsivity $R_V$

$$\delta I_0 = \frac{\beta_e(\delta V_0)}{\Omega_1} L H \left| \frac{\cos \gamma_0 L - \gamma_0 L \sin \gamma_0 L}{\cos \gamma_0 L} \right|^2.$$  

$$R_V = \frac{\beta_e(\delta V_0)}{\Omega_1} L H \left| \frac{\cos \gamma_0 L - \gamma_0 L \sin \gamma_0 L}{\cos \gamma_0 L} \right|^2.$$  

Here the characteristic responsivity $R_V$ is given by

$$R_V = 2\pi c G \left( \frac{\beta_i}{\sigma_0^0} \right) = 2\pi c G \left( \frac{\beta_i V_0}{j_i^2} \right),$$  

where $c$ is the speed of light in vacuum, $G \simeq 1.5$ is the antenna gain factor, $\sigma_0^0 = j_i^0 / V_0$ and $j_i^0$ are the inter-GL dc conductivity and current density, respectively. Considering that at $V_0 = V_t$ (when the RT current exhibits a maximum) above expression yields $\beta_i = j_i^\text{max} / (\Delta V_t)^2$, we arrive at the following formula

$$\frac{R_V}{\Delta V_t^2} \left| \cos \gamma_0 L \right|^2 \left| \frac{\cos \gamma_0 L - \gamma_0 L \sin \gamma_0 L}{\cos \gamma_0 L} \right|^2.$$  

Equation (23) provides the frequency dependence similar to the responsivity $R_V$ of the double-GL detectors using the nonlinearity of the inter-GL relatively smooth current–voltage characteristic with the tunnelling assisted by electron scattering (non-RT detector) considered by us recently [5]. However, there are two distinctions (apart from the difference in the $R_V$ sign). First, the absolute value of $R_V$ is much larger than $R_V$. This is due to a significantly larger value of $|\beta_i|$ in the RT detectors associated with a high and sharp RT peak. Indeed, considering equation (24) and the pertinent equation in [5], one can arrive at

$$R_V = \frac{2\pi c G}{\beta_i V_0} \left( \frac{\beta_i V_0}{\Delta V_t^2} \right).$$

Setting $\Delta V_t = 30–90$ mV and $V_0 = 1000$ mV, we obtain $R_V / R_{V_0} \simeq 10^2–10^3$. At the above parameters, assuming that $j_i^0 = j_i^\text{max}$, one obtains $R_V \simeq (1.5–13.9) \times 10^4$ V W$^{-1}$. Second, the responsivity peaks of the inter-GL RT detector width is characterized by the collision frequency $\nu$ (because $v_t = 0$), but in the detectors using non-RT the width of the peaks is determined by $(v + v_t)$ with $v_t > 0$. The possibility to achieve very high values of the characteristic responsivity $R_V$ is connected with a large value of $\beta_i$ and, hence, small values of the width of tunnelling resonance $\Delta V_t$. One can assume that the latter quantity weakly depends on the temperature [8], so that the responsivity can be very high even at room temperature.

As follows from equation (22), the frequency dependence of the responsivity exhibits sharp maxima at the plasma resonant frequencies $\omega = \omega_0$, where the frequencies $\omega_0$ are given by equation (16). The widths of the peaks are determined by the parameter $\Gamma \propto \nu$ (at the RT resonance $v_t = 0$). At the plasma resonances, $|R_V| \gg R_V$. Thus, very high values of the responsivity of the detectors in question can be achieved due to combining of the tunnelling and plasma resonances.

Since the resonant plasma frequencies fall into the THz range, the detector under consideration can be particularly useful for the resonant detection of THz radiation.

Figure 3 demonstrates examples of the frequency dependences of the responsivity calculated using equation (22) for the double-GL RT structures with different values of the electron and hole collision frequency $\nu$ and different values of the plasma frequency $\Omega$. The obtained dependences of the responsivity versus signal frequency exhibit several resonant peaks associated with the plasma oscillations. The highest peaks correspond to the zeroth resonances at the frequency $\omega_0 < \Omega$, while the other resonances correspond to multiples of the plasma frequency $\Omega$ (see equation (18)). One can see that $R_V > R_{V_0}$ not only at the zeroth plasma resonance, but also a higher resonances. The number of such resonances depends on the quality factor $Q$. The responsivity is very high due RT with sharp maximum at the current voltage-characteristics even at the moderate quality factors. However, it is much higher at the pronounced plasma resonances.

The high values of the responsivity with the frequency characteristics of figure 3 are associated with the combination of the tunnelling and plasma resonances. The deviation from the tunnelling resonance leads to lowering of the responsivity.

If $V_0 \neq V_t$, the factor $R_V$ in equation (22) becomes smaller than $R_{V_0}$:

$$R_V = \frac{R_{V_0}}{\Delta V_t^2} \left[ \left( \frac{V_0 - V_t}{\Delta V_t} \right) - 1 \right] \times \exp \left[ - \left( \frac{V_0 - V_t}{\Delta V_t} \right)^2 \right].$$

(26)
Figure 4. Dependence of normalized responsivity $R_V / \Omega_1$ versus bias voltage swing $(V_0 - V_t) / \Delta V_1$ at different signal frequency $\omega$ near the zeroth plasma resonance (upper panel) and near the first plasma resonance (lower panel).

Figure 4 shows the dependences of the normalized responsivity, $R_V / \Omega_1$, on the voltage swing $(V_0 - V_t) / \Delta V_1$, calculated using equation (26) for different signal frequencies in the vicinity of the zeroth and first plasma resonances. The plasma frequency at $V_0 = V_t$ was chosen to be $\Omega_0 / 2\pi = 3.0$ THz. The plasma frequency at different values of $V_0$ is given by $\Omega = \Omega_0 [1 + (V_0 - V_t) / \bar{V} 0]^{1/4}$, where $\bar{V}_0 = 4\pi e d / \kappa \Sigma_1$. At $\kappa = 4$, $d = 4$ nm, and $\Sigma_1 = (1-5) \times 10^{12}$ cm$^{-2}$, $\bar{V}_0 \sim 180$–900 mV. We set $\bar{V}_0 / \Delta V_1 = 6$ and $\nu = 0.5 \times 10^{12}$ s$^{-1}$. As seen from figure 4, an increase in the absolute value of the voltage swing $|V_0 - V_t| / \Delta V_1$ results in a marked drop of the responsivity. It is also seen that detuning of the plasma resonance leads to a significant decrease in the responsivity (compare the curves for the plasma resonances at $\omega / 2\pi = 0.82$ THz and $\omega / 2\pi = 3.27$ THz with those corresponding to a detuning $\Delta \omega / 2\pi = \pm 0.08$ THz. Slightly different maximum values of the responsivity shifted from the plasma resonances are due to a small asymmetry of the resonant peaks. Different positions of these maxima are associated with the dependence of the plasma frequency on $V_0$.

The excitation of plasma oscillation by electromagnetic signals can be used not only for the resonant reinforcement of the rectified current (i.e., the detector responsivity), but also for a more effective generation of higher harmonics [8].

5. Conclusions

In summary, we considered the dynamic behaviour of the double-GL RT structures. We calculated the frequency-dependent admittance and the responsivity of the double-GL RT structures to the incoming signals as functions of the structural parameters, bias voltages, and frequency. It was demonstrated that the stationary states of the electron–hole plasma are stable with respect to the self-excitation of plasma oscillations and aperiodic perturbations for the structures with realistic parameters. As shown, the responsivity exhibits sharp resonant maxima corresponding to the excitation of plasma modes by incoming electromagnetic radiation. The plasma oscillations and the pertinent responsivity peaks are in the THz range. The responsivity of the double-GL RT detectors operating at room temperature can exhibit very high values markedly exceeding $(10^{2}–10^{3}) \text{V W}^{-1}$.

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References

[1] Liu M, Yin X, Ulin-Avila E, Geng B, Zentgraf T, Ju L, Wang F and Zhang X 2011 Nature 474 64
[2] Britnell L et al 2012 Science 335 947
[3] Liu M, Yin X and Zhang X 2012 Nano Lett. 12 1482
[4] Georgiou T et al Nature Nanotechnol. 8 100
[5] Ryzhii V, Otsuji T, Ryzhii M and Shur M S 2012 J. Phys. D: Appl. Phys. 45 302001
[6] Ryzhii V, Ryzhii M, Mitin V, Shur M S, Satou A and Otsuji T 2013 J. Appl. Phys. 113 174506
[7] Feenstra R M, Jena D and Gu G 2012 J. Appl. Phys. 111 043711
[8] Zhao P, Feenstra R M, Gu G and Jena D 2013 IEEE Trans. Electron Devices 60 951
[9] Vasko F T 2013 Phys. Rev. B 87 075424
[10] Britnell L, Gorbatchev R V, Geim A K, Ponomarenko L A, Mishchenko A, Greenaway M T, Fromhold T M, Novoselov K S and Eaves L 2013 Nature Commun. 4 1794
[11] Luryi S 1988 Appl. Phys. Lett. 52 501
[12] Svintsov D, Vyurkov V, Yurchenko S, Otsuji T and Ryzhii V 2012 J. Appl. Phys. 111 083715
[13] Shur M 1990 Physics of Semiconductor Devices (Englewood Cliffs, NJ: Prentice-Hall)
[14] Ryzhii V, Satou A and Otsuji T 2007 J. Appl. Phys. 101 024509
[15] Rudin S 2011 Int. J. High Speed Electron. Syst. 20 567
[16] Stauber T and Gomez-Santos G 2012 Phys. Rev. B 85 075410
[17] Zhu J-J, Badalyan S M and Peters F M 2013 Phys. Rev. B 87 085401
[18] Ryzhii V 2006 Japan. J. Appl. Phys. 45 L923
[19] Ryzhii V and Shur M 2001 Japan J. Appl. Phys. 40 546
[20] Kanaya H, Shibayama H, Sogabe R, Suzuki S and Asada M 2012 Appl. Phys. Express 5 124101