LETTER TO THE EDITOR

On the correlation between stellar chromospheric flux and the surface gravity of close-in planets

A. F. Lanza

ABSTRACT

Aims. The chromospheric emission of stars with close-in transiting planets has been found to correlate with the surface gravity of their planets. Stars with low-gravity planets have on average a lower chromospheric flux.

Methods. We propose that this correlation is due to the absorption by circumstellar matter that comes from the evaporation of the planets. Planets with a lower gravity have a greater mass-loss rate which leads to a higher column density of circumstellar absorption and this in turn explains the lower level of chromospheric emission observed in their host stars. We estimated the required column density and found that planetary evaporation can account for it. We derived a theoretical relationship between the chromospheric emission as measured in the core of the Ca II H&K lines and the planet gravity.

Results. We applied this relationship to a sample of transiting systems for which both the stellar Ca II H&K emission and the planetary surface gravity are known and found a good agreement, given the various sources of uncertainties and the intrinsic variability of the stellar emissions and planetary evaporation rates. We consider implications for the radial velocity jitter applied to fit the spectroscopic orbits and for the age estimates of planetary systems based on the chromospheric activity level of their host stars.

Key words. planetary systems – stars: activity – stars: chromospheres – circumstellar matter

1. Introduction

Main-sequence late-type stars have outer convection zones where turbulence excites sound waves. They dissipate in the outermost low-density regions of the atmosphere, leading to the formation of a chromosphere, that is, a layer where temperature increases outwards. In addition to this basal acoustic heating, the energy dissipated by magnetic fields, which are produced by a hydromagnetic dynamo in the convection zone, contributes to the chromospheric emission. In active stars, magnetic heating dominates the basal heating by orders of magnitude, leading to a wide range of chromospheric emission levels in stars with similar effective temperature and mass (e.g., Ulmschneider et al. 1991).

Considering a sample of transiting planets, Hartman (2010) (hereafter H10) and Figueira et al. (2014) found an intriguing correlation between the chromospheric emission of their hosts and the surface gravity of the planets, in which the emission is lower for stars with planets with a lower surface gravity. A suggestion to explain such a correlation came from the observations of Haswell et al. (2012) and Fossati et al. (2013). They found a complete lack of emission in the cores of the Mg II h&k and Ca II H&K lines in WASP-12 and attributed this to the absorption of circumstellar matter probably coming from the evaporation of the planet.

In this Letter, we propose a mechanism based on the evaporation and subsequent condensation of matter from a close-in planet to explain the correlation found by H10.

2. Observations

We consider transiting exoplanetary systems with both measured chromospheric emission and planetary surface gravity. Chromospheric emission is measured by the $R'_{\text{HK}}$ index (e.g., Knutson et al. 2010). It is determined by computing the chromospheric index $S$, which is the ratio of the flux measured in the cores of the Ca II H&K lines using triangular passbands with a FWHM of 1 Å to the flux in two reference passbands of 20 Å centred on the continuum of the lines. The $S$ index is converted into a standard scale and corrected for the residual photospheric emission, leading to a non-dimensional measure of the chromospheric emission called $R'_{\text{HK}}$. When a given star has several observations, the median value of log $R'_{\text{HK}}$ is adopted.

The planetary surface gravity $g$ comes directly from the spectroscopic orbit and the transit lightcurve, without constraints from stellar or atmospheric models (Southworth et al. 2007). We added 15 new transiting planets to the sample of H10 with gravity and log $R'_{\text{HK}}$ as listed in the exoplanets.org database on 16 October 2014 (Wright et al. 2011), this makes a total of 54 systems. The mass $M$ and orbital semimajor axis $a$ of our planets and the effective temperature $T_{\text{eff}}$ of their hosts were taken from exoplanets.org. Several planets listed by H10 have no log $R'_{\text{HK}}$ value in that database, therefore we took log $R'_{\text{HK}}$ from H10 when available, while $g$ and its uncertainty came from exoplanets.org. For WASP-18, we adopted log $R'_{\text{HK}} = -5.153$ (see Isaacson, private communication, and Miller et al. 2012).

3. Model

3.1. Configuration of the stellar coronal field

In the Sun, prominences form by condensing plasma as a result of a thermal instability in long magnetic loops which have a dip close to their top where matter can be accumulated without falling under the action of gravity. The matter that forms a prominence probably comes from the evaporation of the chro-
mosphere induced by magnetic heating that is localized close to the footpoints of the long loop (cf. [Lanza et al. 2001] and references therein). Rapidly rotating late-type stars such as AB Dor show signatures of condensations absorbing in Hα, that are located a few stellar radii above the surface (Collier Cameron & Robinson 1989a,b). Prominence-like structures were also observed in CoRoT-2 (Czesla et al. 2012).

In late-type stars that are accompanied by close-in planets, different magnetic configurations are possible, including some that are capable of sustaining plasma condensations against the stellar gravitational field. Lanza (2009, 2012) introduced coronal field models and described their properties. Linear force-free fields represent the minimum energy configuration for a given total magnetic helicity that is attained thanks to the continuous energy dissipation associated with the reconnection between the coronal and the planetary fields as the planet orbits the star. Some linear force-free fields have closed field lines that are suitable to store the condensed plasma, as shown in Fig. 1 for an axisymmetric field with some azimuthal twist (see Lanza 2009 for details). At a distance of a few stellar radii from the star, there are field lines with dips where the gravitational potential has a relative minimum which allows storing condensed matter. The very long loops make thermal conduction ineffective, so the condensed plasma cannot be re-heated by the hot stellar corona, and the stellar radiation cannot re-evaporate the matter because the absorption of the Lyman continuum requires column densities orders of magnitude greater than expected in those structures (see Sect. 3.2). Therefore, it is conceivable that, once formed, plasma condensations at chromospheric temperatures can remain stable. The weight of the stored material helps to stabilize the whole configuration because a sizable change of the field line geometry would lift up the matter which in turn would require additional energy (cf. Lanza 2009). For the same reason, large quiescent solar prominences are the most long-lived structures in the solar corona with lifetimes that can reach ten months.

3.2. Absorption of the chromospheric flux by circumstellar condensations

As observed in the Sun, the thermal instability by which condensations are formed produces clumps of relatively low-temperature material that is separated by regions of higher temperature and lower density in approximately pressure equilibrium. Therefore, we do not expect that the azimuthal flux rope encircling the star is uniformly filled with a homogeneous condensation, but that several clumps of material are formed inside it. They absorb at different wavelengths because of their individual radial velocities. Since the matter comes from the evaporating planet, it initially has its orbital angular momentum. To allow it to condense closer to the star inside a coronal field that rotates with the stellar angular velocity, this matter must give up some of its initial angular momentum which is transferred to the star by magnetic stresses. However, since the core magnetic field has an azimuthal component, the condensed plasma can flow in the azimuthal direction along the magnetic field lines and acquire azimuthal velocities up to several times of km s⁻¹ thanks to the initial angular momentum it had when it left the planet. In conclusion, we expect to find prominences capable of absorbing all along the 1 Å intervals centred on the cores of the Ca II H&K lines used to measure the chromospheric index. Vial (1982a,b) observed and modelled several intense lines in solar prominences. We adopted his radiation transfer model to estimate the optical depth τ₀ at the central wavelengths of the Ca II H&K lines across a slab of condensed matter of thickness X, with a typical temperature of 8 × 10⁶ K, electron density 2 × 10¹⁰ cm⁻³, and a hydrogen ionization fraction n_p/n_e = 3, where n_p is the number density of the protons and n_e that of the hydrogen atoms in the fundamental state. A microturbulence velocity of 8 km s⁻¹ was adopted. Assuming solar abundance for Ca, the hydrogen column density corresponding to τ₀ = 1 in the core of the Ca II K line is N_H = 1.8 × 10¹⁸ cm⁻², while for the Ca II H line it is N_H = 3.5 × 10¹⁸ cm⁻². The FWHM of the lines is ~ 0.2 Å, implying that at least five absorbing clumps with radial velocities within ±40 km s⁻¹ of the stellar radial velocity are needed to uniformly absorb along the 1 Å windows where the chromospheric emission is measured.

The observed range of R′_c in our sample of stars covers about one order of magnitude (cf. Sect. 4 and Fig. 2) implying that the highest absorption of the flux is about a factor of ten, corresponding to an average optical depth across the 1 Å windows of τ ≈ 2.5. This implies a total hydrogen column density, considering all the five different clumps absorbing at different radial velocities, of ~ 4.4 × 10¹⁹ cm⁻² for the Ca II H line and half that value for the Ca II K line. We estimated the total amount of matter into the condensations by assuming that it is stored in a cylindrical slab of base radius r_t that extends in the direction parallel to the axis of symmetry for at least 2R_s, where R_s is the radius of the star, to completely cover the stellar disc. Therefore, the volume filled with the condensations is approximately V = 4π r_t R_s X, where X ≪ R_s is their typical thickness. Following Fig 1 we assume r_t ~ 2.5 R_s. For X = 5 × 10⁸ cm, we need an average hydrogen density of n = 8.8 × 10¹⁰ cm⁻³ to account for the highest total absorption. For an F-type star, R_s ~ 10¹¹ cm, hence V ~ 1.6 × 10³² cm³ and the total high-
The mass-loss rate is powered by the stellar extreme-ultraviolet flux $F_{\text{EUV}}$ (cf. Lecavelier des Etangs 2007) and can be estimated by assuming that the flux received by the planet $\pi F_{\text{EUV}}(R_{\ast}/a)^2 R^2$ is converted into work against its gravitational field with an efficiency $\eta$ (e.g., Forcada et al. 2011), that is,

$$M = \pi \eta F_{\text{EUV}} \left( \frac{R_{\ast}}{a} \right)^2 \frac{R^2}{GM},$$

$$= \pi \eta F_{\text{EUV}} \left( \frac{R_{\ast}}{a} \right)^2 g^{-1} R,$$

(5)

where $G$ is the gravitation constant and we have explicitly introduced the surface gravity $g = GM/R^2$. Substituting Eqs. (5), (4), and (3) into Eq. (2), we obtain an expression for the mean optical depth $\tau$ and recast Eq. (1) as

$$\log R'_{\text{HK}} = \log R''_{\text{HK}} - \gamma g^{-1},$$

(6)

where $\gamma \equiv 0.0434 (a \eta F_{\text{EUV}})/(m_p c_s)$ depends on the stellar high-energy radiation and the temperature of the evaporation flow that determines the sound speed.

### 4. Results

In Fig. 2 we plot the stellar chromospheric index $\log R'_{\text{HK}}$ vs. the inverse of the surface gravity of the planet. H10 considered a subsample with $M > 0.1 M_{\odot}$, $a < 0.1$ AU and 4200 < $T_{\text{eff}}$ < 6200 K because they have calibrated values of $R''_{\text{HK}}$ and better determined parameters (his subsample 1). We used the same criteria for selecting our corresponding subsample, finding 31 planets that are plotted in Fig. 2 with filled dots. The red dashed line is the linear regression

$$\log R'_{\text{HK}} = -(4.43 \pm 0.07) - (532 \pm 78) g^{-1},$$

(7)

where $g$ is in cm s$^{-2}$ and the uncertainties correspond to one standard deviation. They were computed by assuming a standard deviation of 0.12 for $\log R''_{\text{HK}}$ as a result of measurement and conversion errors (Knutson et al. 2010), and stellar activity cycles. In the Sun, the peak-to-peak variation along the 11-yr cycle amounts to $\Delta \log R''_{\text{HK}} \sim 0.24$ (Baliunas et al. 1995) and can be assumed as typical for stars with a low activity level which is the case of most of our planet hosts.

The Spearman correlation coefficient is $-0.61$ with a probability of chance occurrence of 0.030 percent. We obtain a chi square of 124.4 for the best fit in Eq. (7). The fit residuals are higher than expected on the basis of the data uncertainties and can be explained by considering the differences in the intrinsic EUV flux, and, to a lesser extent, in the evaporation flow temperatures of different planets that make the parameter $\gamma$ remarkably variable from one planet to the other. For example, in the Sun, $F_{\text{EUV}}$ varies by a factor of $\approx 3 - 4$ along the 11-yr cycle, and larger variations are observed during major stellar flares, which affect planetary evaporation rates (Lecavelier des Etangs et al. 2012). We estimate the mean $F_{\text{EUV}}$ from the slope $\gamma = 532$ cm s$^{-2}$, adopting $\alpha = 2.9 \times 10^{-19}$ cm$^2$, corresponding to solar abundance, $\eta = 0.5$, and $c_s = 15$ km s$^{-1}$, that is, a temperature of $\sim 10^4$ K for the evaporation flow. We find $F_{\text{EUV}} = 4.7$ erg cm$^{-2}$ s$^{-1}$ at the distance of 1 AU, similar to the mean $F_{\text{EUV}}$ of the Sun (cf. Lecavelier des Etangs 2007). Note that our model implicitly assumes $R''_{\text{HK}}$ to be the same for all the stars, so the correlation should become stronger if $R''_{\text{HK}}$ were individually known together with $F_{\text{EUV}}$ and $c_s$.

We also computed a linear regression for our complete sample of 54 data points, corresponding to subsample 3 of H10. It is plotted as a dot-dashed line in Fig. 2 with intercept $-4.72 \pm 0.04$ and slope $\gamma = -257 \pm 43$ cm s$^{-2}$. The remarkable variation of
The red dashed line is a linear regression computed by considering the 31 data points (filled circles) with $M > 0.1 \, M_\odot$, $a < 0.1 \, \text{AU}$ and stellar effective temperature $4200 < T_{\text{eff}} < 6200 \, \text{K}$. The red dot-dashed line is a linear regression computed with the entire set of 54 datapoints. Those not included in the restricted sample are indicated by open circles. Note that the point corresponding to WASP-17b (an open circle) is outside the scale of the plot, but it is included in the regression. The three-dots-dashed blue lines are the theoretical relationship for the Sun (the line with the lower slope) and for the illustrative case of a star with twice the solar chromospheric and $F_{\text{EUV}}$ fluxes.

The regression line parameters arises because several datapoints fall below the regression for $g^\prime < 0.0005 \, \text{cm}^{-1} \, \text{s}^{-2}$.

To allow for a preliminary comparison with our theory, we plot Eq. (5) in Fig. 2 with the above constant values for $\alpha$, $\eta$, $c_s$, and assuming mean solar flux values, that is $\log P_{\text{HK}}^0 = -4.875$ and $F_{\text{EUV}} = 4.64 \, \text{erg cm}^{-2} \, \text{s}^{-1}$ at 1 AU, or twice solar flux values, to illustrate the case of a sun-like or of a more active star, respectively. The intercepts of those theoretical regression lines are smaller than those found by fitting the data points, suggesting that most of the sample stars are remarkably more chromospherically active than the Sun. On the other hand, the slopes are similar, that is, their average $F_{\text{EUV}}$ is similar to the Sun’s.

H10 and Figueira et al. (2014) plotted $\log R_{\text{HK}}^0$ vs. $\log g$ instead of our physically motivated relationship. The chi square of the linear regression between $\log R_{\text{HK}}^0$ and $\log g$ is 117.1 for subsample 1, giving no significant preference for this functional form with respect to that we adopted. Finally, the Spearman correlation coefficient between $\log R_{\text{HK}}^0$ and $a$ is $-0.19$ corresponding to a probability of a chance association of $\sim 30$ percent (cf. Sect. 3.3 and Appendix A).

5. Discussion and conclusions

We propose an explanation for the correlation between the stellar chromospheric emission and the surface gravity of close-in exoplanets (H10 and Figueira et al. 2014). It is based on the absorption by prominence-like structures around the host star formed by the plasma evaporating from the planet (Lanza 2009). The observations of WASP-12 by Haswell et al. (2012) and Fossati et al. (2013) provide support to the proposed mechanism. WASP-12 is an extreme system in terms of closeness of its hot Jupiter to its Roche lobe, which should strongly enhance its evaporation rate. This agrees with the fact that its $\log R_{\text{HK}}^0$ is the lowest of our sample.

The possibility that a low $R_{\text{HK}}^0$ indicates an intrinsic low activity level in some of our stars cannot be excluded. Pillet et al. (2014) found that circumstellar absorption cannot explain the low level of X-ray emission in WASP-18, contrary to the suggestion by Fossati et al. (2014). The strong tides generated on the star by such a massive and close-in planet might significantly affect the stellar dynamo and remarkably reduce its activity. On the other hand, evidence for hot Jupiters spinning up their hosts was found by Poppenhaeger & Wolf (2014) in CoRoT-2 and possibly HD 189733.

The evolution of the intrinsic chromospheric emission is significant only during the first $\sim 2$ Gyr on the main sequence (Pace 2013), which means that it does not greatly affect our sample that mainly consists of solar-age stars. Moreover, planetary mass loss through evaporation, even at a rate of $10^{12} \, \text{g} \, \text{s}^{-1}$, has a limited effect on Jupiter-mass objects. We refer to H10 for more considerations on evolutions that affect the results.

A consequence of our model is that a measure of the chromospheric emission cannot be immediately taken as a proxy for the photospheric activity level of a planet-hosting star. The intrinsic activity can be significantly higher than derived from $R_{\text{HK}}^0$, and this can affect the estimate of the radial-velocity jitter term included when fitting the spectroscopic orbit of a transiting planet. Age estimates based on the chromospheric emission level (e.g., Mamajek & Hillenbrand 2008) can lead to systematically older values than the true ages for stars with low-gravity planets.

We implicitly assumed alignment between the stellar spin, the axis of symmetry of the coronal field that supports the condensations, and the orbital angular momentum. However, a misalignment between the stellar spin and the orbital angular momentum is observed in several systems, particularly when $T_{\text{eff}} \gtrsim 6200 \, \text{K}$ (Albrecht et al. 2012). This suggests that systems with an inclination different from 90° may also display effects of circumstellar absorption.

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Appendix A: Alternative scalings for the optical depth

Alternative scalings to those adopted in Sect. 3.3 can be considered. In our hypotheses, the total volume $V$ is independent of the orbit semimajor axis $a$ because the size of the region enclosing the relative minimum of the gravitational potential along the magnetic field lines scales with the radius of the star $R_*$, given that the boundary conditions controlling the field geometry are fixed at the surface of the star. Therefore, we expect that in general the vertical extension of the slab depends on $R_*$ rather than the distance $a$ of the planet. In other words, the volume $V$ should be proportional to $R_*^2X$ although the coefficient of proportionality is not necessarily that adopted above, that is, $4\pi \times 2.5$, which corresponds to the smallest vertical extension of the slab $\sim 2R_*$.

The shortest possible timescale corresponds to the free-fall time in the case of negligible pressure gradients and Lorentz force, and neglecting the ram pressure of the stellar wind. In this case, $t_a = \sqrt{2\pi (GM_*)^{-1/2}a^{3/2}}$, where $M_*$ is the mass of the star, and the optical depth appearing in Eq. (1) becomes

$$\tau = \sqrt{2\pi \frac{\alpha \eta F_{\text{EUV}} 10^{-10}}{M_p} \sqrt{\frac{M}{M_*}} a^{-3/2} g^{-1/2}}. \quad (A.1)$$

Conversely, the longest timescale is that given by the diffusion process considered in Sect. 3.3. An intermediate possibility is that of a syphon flow along the magnetic field lines that directly carries the evaporated matter into the potential well. The typical velocity of that flow is of the order of the sound speed $c_s$ (cf. the evaporation model in the presence of planetary and stellar magnetic fields by Adams 2011), thus $t_a \sim a/c_s$. With that scaling, we find

$$\tau \sim \frac{\alpha \eta F_{\text{EUV}} 10^{-10}}{M_p} c_s \left( \frac{R}{a} \right) g^{-1}, \quad (A.2)$$

where $c_s$ is constant in the case of a steady isothermal flow.