Research Article

Investigation on Boron Alpha Nanotube by Studying Their M-Polynomial and Topological Indices

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Graph theory provides an effective tool such as graph polynomial and topological indices (TIs) to the chemist to analyze the different chemical structures. TIs are the numerical entity deducted from the molecular structure. TI helps to study the relationship between the physicochemical properties and structure of the chemical compound. In this article, we investigate the boron α-nanotube by computing its M-polynomial and then deducing its TI. Results are also shown by plotting the graphs.

1. Introduction

Chemical graph theory plays an important role in analysis, designing, interpreting, modeling, and understanding chemical substances. The molecular graph is composed of vertices (atoms) and edges (chemical bonds). Chemical graph theory has many applications during the study of chemical substances [1, 2]. The chemical graph theory provides different tools for mathematical modeling of molecular structure. This modeling is useful for the analysis of chemical compounds. The analysis of chemical compounds is made conceivable by using topological indices (TIs). A large number of TIs are introduced and applied to study pharmacology and theoretical chemistry [3, 4].

The first TI which correlated with the boiling points of alkanes was introduced by H. Wiener called the Wiener index in 1947 [5]. Until now, thousands of indices are designed and used in chemical graph theory [6]. A degree-dependent topological index for the graph $G$ is defined as follows:

\[ I(G) = \sum_{e=xy \in E_G} f(dx, dy). \quad (1) \]

Equation (1) is rewritten by counting the same end-degree edges in chemical graph as follows:

\[ I(G) = \sum_{j \leq k} m_{jk} f(j, k), \quad (2) \]

where $\{dx, dy\} = \{j, k\}$ and the total number of edges $xy$ is denoted by $m_{jk}$. Some important TIs are described in [7]. Reduced reciprocal Randić index [8] is defined as

\[ RRR(G) = \sum_{xy \in E_G} \sqrt{(dx - 1)(dy - 1)}. \]

The first arithmetic-geometric index [9] is defined as

\[ AG_1(G) = \sum_{xy \in E_G} \frac{dx + dy}{2} \sqrt{dx \cdot dy}. \]

SK indices [10] are defined as

\[ SK(G) = \sum_{xy \in E_G} dx + dy/2, \quad SK_1(G) = \sum_{xy \in E_G} dx \cdot dy/2, \quad \text{and} \quad SK_2(G) = \sum_{xy \in E_G} (dx + dy/2)^2. \]

The first Zagreb index in terms of edge degree [11] is defined as

\[ EM_1(G) = \sum_{xy \in E_G} (dx + dy - 2)^2. \]
index [12] is described as $SCI(G) = \sum_{xy \in E_G} 1/\sqrt{d_x + d_y}$. Redefined third Zagreb index [13] is commuted as $ReZG_3(G) = \sum_{xy \in E_G} (d_x d_y (d_x + d_y))$.

Graph polynomials are the best way to represent a chemical graph in chemical graph theory. In this paper, we study the M-polynomial to analyze the chemical structure. M-polynomial gives the TIs by applying some derivatives and integration operations [7, 14]. In 2015, M-polynomial is introduced in [15]. TIs via M-polynomial is extensively calculated by many researchers nowadays [14, 16, 17]. M-polynomial for the graph $G$ is defined as follows:

$$M_G(u, v) = \sum_{v \in V, j \in \Psi} m_{\alpha} u^j v^k.$$  (3)

Here, $\psi = \min\{d_x | x \in V_G\}$ and $\Psi = \max\{d_x | x \in V_G\}$. Closed form via M-polynomial of TI is mentioned in Table 1.

The operators used are defined as follows:

\[
\begin{align*}
D_{\nu}^{1/2} M_G(u, v) &= \sqrt{v} \frac{\partial}{\partial \nu} M_G(u, v) \cdot \sqrt{M_G(u, v)}, \quad D_{\nu}^{1/2} M_G(u, v) = v \frac{\partial}{\partial \nu} M_G(u, v), \\
D_{\nu}^{1/2} M_G(u, v) &= \sqrt{u} \frac{\partial}{\partial \nu} M_G(u, v) \cdot \sqrt{M_G(u, v)}, \quad D_{\nu}^{1/2} M_G(u, v) = u \frac{\partial}{\partial \nu} M_G(u, v), \\
S_{\nu}^{1/2} M_G(u, v) &= \int_0^v \frac{M_G(u, t)}{t} dt \cdot \sqrt{M_G(u, v)}, \quad S_{\nu}^{1/2} M_G(u, v) = u \sqrt{M_G(u, v)}, \quad Q_{\nu}^{1/2} M_G(u, v) = u^2 M_G(u, v).
\end{align*}
\]

2. Chemical Graph of Boron α-Nanotube

The search for small size, low cost, and high efficient materials is the most intersecting topic nowadays. To get this goal, there is a need to study the chemical and physical behavior of chemical substances. So, nanotechnology becomes the most important field in the twenty-first century. By using the chemical graph theory technique, nanostructures are transformed into a mathematical model and then inspected under numerous parameters. Due to attractive features such as work function, transport property, electronic structure, and structural stability, boron α-nanotubes have gained an important place in modern times [18, 19]. The boron α-nanotube is constructed by boron α-nanosheet consisting of $q$ column and $l$ rows. There are three methods to connecting the first and last column of boron α-nanosheet: armchair, zigzag, and chiral [20].

On the basis of rows, there are two types of boron α-nanotube such as $l \equiv 0 \pmod{3}$ shown in Figure 1(a) and $l \equiv 2 \pmod{3}$ shown in Figure 1(b). In the present study, we consider the armchair connecting of boron α-sheet to form a boron α-nanotube for $l \equiv 0 \pmod{3}$ and symbolize as $B_{\alpha NT_{l0}}$ shown in Figure 2. Vertex partition of $B_{\alpha NT_{l0}}$ is presented in Table 2, and edge partition is in Table 3.

3. M-Polynomial and Topological Indices of Boron α-Nanotube

Theorem 1. If $B_{\alpha NT_{l0}}$ represents a boron α-nanotube, then $M$-polynomial of $B_{\alpha NT_{l0}}$ is $M_{B_{\alpha NT_{l0}}}(u, v) = q/2u^5 v^3 + qu^3 v^5 + qu^2 v^6 + 3q/2u^2 v^4 + 2qu^4 v^2 + qu^4 v^6 + q/2(3l - 8)u^2 v^5 + q(2l - 8)u^5 v^6$ [21, 22].

Theorem 2. Let $B_{\alpha NT_{lq}}$ represent the boron α-nanotube and $M_{B_{\alpha NT_{lq}}}(u, v) = q/2u^5 v^3 + qu^3 v^5 + qu^2 v^6 + 3q/2u^2 v^4 + 2qu^4 v^2 + qu^4 v^6 + q/2(3l - 8)u^2 v^5 + q(2l - 8)u^5 v^6$. Then,

(1) $RRR_{[B_{\alpha NT_{lq}}]} = (6 + 4\sqrt{5})ql - 1/2 (21 - 4 \sqrt{2} - 8 \sqrt{3} + 20 \sqrt{5} - 2 \sqrt{10} - 2 \sqrt{15})q$

(2) $AG_{[B_{\alpha NT_{lq}}]} = 1/30 (45 + 11 \sqrt{30})ql + 1/60 (45 \sqrt{2} + 54 \sqrt{5} + 25 \sqrt{6} + 16 \sqrt{12} - 55 \sqrt{30} - 120)q$

(3) $SK_{[B_{\alpha NT_{lq}}]} = 37/2ql - 35/2q$

(4) $SK_{1[B_{\alpha NT_{lq}}]} = 195/4ql - 249/4q$

(5) $SK_{2[B_{\alpha NT_{lq}}]} = 98ql - 121q$

(6) $EM_{1[B_{\alpha NT_{lq}}]} = 258ql - 352q$

(7) $SCI_{[B_{\alpha NT_{lq}}]} = 1/220 (33 \sqrt{10} + 40 \sqrt{11})ql + 1/1320 (1320 + 825 \sqrt{2} + 110 \sqrt{6} - 396 \sqrt{10} - 600 \sqrt{11})q$
Table 1: Topological indices derived from $M_G(u, v)$.

| Topological index | Derivation from $M_G(u, v)$ |
|-------------------|-----------------------------|
| RRR$[G]$         | $D_u^{1/2}D_v^{1/2}Q_{u-1, v-1}M_G(u, v)|_{u=v=1}$ |
| AG$_1[G]$        | $1/2D_u^{-1/2}S_u^{1/2}M_G(u, v)|_{u=1}$ |
| SK$_1[G]$        | $1/2(D_u + D_v)M_G(u, v)|_{u=v=1}$ |
| Sk$_1[G]$        | $1/2D_u^{-1/2}D_v^{-1/2}M_G(u, v)|_{u=v=1}$ |
| EM$_1[G]$        | $D_u^2Q_{u-1, -1}M_G(u, v)|_{u=1}$ |
| SCI$[G]$         | $S_u^{1/2}M_G(u, v)|_{u=1}$ |
| SCI$_1[G]$       | $D_u^1M_G(u, v)|_{u=1}$ |
| ReZG$_3[G]$      | $D_uD_v(D_u + D_v)M_G(u, v)|_{u=v=1}$ |

(a) 12 34 56 q1
column
1 2 3 4 5 6 7 8 9
l
Rows

(b) 1 2 3 4 5 6 7 8 9
column

Figure 1: Boron $\alpha$-nanosheet $B_\alpha NS_{lq}$: (a) $l \equiv 0 \pmod{3}$; (b) $l \equiv 2 \pmod{3}$.

Table 2: Vertex partition of boron $\alpha$-nanotube ($B_\alpha NT_{lq}$).

| $d_x$ | 3 4 5 6 | Total vertices |
|-------|---------|----------------|
| Number of vertices | $q$ | $3/2q$ | $q(l - 2)$ | $1/6q(2l - 3)$ | $4/3ql$ |

Figure 2: Boron $\alpha$-nanotube ($B_\alpha NT_{lq}$).
Table 3: Edge partition of boron α-nanotube \( (B_{α}NT_{4q}) \).

| \((d_k, d_q)\) | Number of edges |
|----------------|-----------------|
| (3,3)          | 1/2q            |
| (3,5)          | q               |
| (3,6)          | q               |
| (4,4)          | 3/2q            |
| (4,5)          | q               |
| (4,6)          | q               |
| (5,5)          | 1/2q(3l - 8)    |
| (5,6)          | q(2l - 5)       |
| Total edges    | 1/2q(7l - 4)    |

\( (8) \) \( SCI \{ B_{α}NT_{4q} \} = 1/2( 3 \cdot 10^3 + 4 \cdot 11^3 )q l + 1/2( 6^3 \) + Proof.
\( 5 \cdot 8^3 + 6 \cdot 9^3 - 6 \cdot 10^3 - 10 \cdot 11^3 )q \)
\( (9) \) \( ReZG_{j} (B_{α}NT_{4q}) = 1035ql - 1549q \)

\( Q_{\nu(-1)} M_{B_{α}NT_{4q}} (u, v) = \frac{q}{2} u^2 v^2 + qu^3 v^4 + qu^3 v^5 + \frac{3q}{2} u^4 v^3 + 2qu^4 v^4 + qu^4 v^5 + \frac{q}{2} (3l - 8)u^5 v^4 + q(2l - 8)u^5 v^5 , \)

\( Q_{\nu(-1)} Q_{\nu(-1)} M_{B_{α}NT_{4q}} (u, v) = \frac{q}{2} u^2 v^2 + qu^3 v^4 + qu^3 v^5 + \frac{3q}{2} u^4 v^3 + 2qu^4 v^4 + qu^4 v^5 + \frac{q}{2} (3l - 8)u^4 v^4 + q(2l - 8)u^4 v^5 , \)

\( D^{1/2}_v Q_{\nu(-1)} Q_{\nu(-1)} M_{B_{α}NT_{4q}} (u, v) = \frac{\sqrt{2}}{2} qu^2 v^2 + qu^2 v^4 + \sqrt{5}qu^3 v^5 + \frac{3\sqrt{2}}{2} qu^3 v^3 + 4qu^4 v^4 + \sqrt{5} qu^3 v^5 + q(3l - 8)u^4 v^4 + \sqrt{5} q(2l - 8)u^4 v^5 , \)

\( D^{1/2}_v D^{1/2}_v Q_{\nu(-1)} Q_{\nu(-1)} M_{B_{α}NT_{4q}} (u, v) = qu^2 v^2 + 2\sqrt{2} qu^2 v^4 + \sqrt{10}qu^2 v^5 + \frac{9}{2} qu^3 v^3 + 4\sqrt{3}qu^3 v^4 + \frac{\sqrt{15}qu^3 v^5}{2} + 2q(3l - 8)u^4 v^4 + 2\sqrt{5}q(2l - 8)u^4 v^5 , \)

\( S^{1/2}_v M_{B_{α}NT_{4q}} (u, v) = \frac{\sqrt{3}}{6} qu^3 v^3 + \frac{\sqrt{5}}{5} qu^3 v^5 + \frac{\sqrt{6}}{6} qu^3 v^6 + \frac{3}{4} qu^4 v^4 + \frac{2\sqrt{5}}{5} qu^4 v^5 + \frac{\sqrt{6}}{6} qu^4 v^6 + \frac{\sqrt{15}qu^3 v^5}{10} + \frac{\sqrt{2}}{6} qu^3 v^6 + \frac{3}{8} qu^4 v^4 + \frac{\sqrt{5}}{5} qu^4 v^5 + \frac{\sqrt{6}}{6} qu^4 v^6 + \frac{1}{10} q(3l - 8)u^5 v^5 + \frac{\sqrt{30}}{30} q(2l - 8)u^5 v^6 , \)

\( S^{1/2}_u S^{1/2}_v M_{B_{α}NT_{4q}} (u, v) = \frac{1}{6} qu^3 v^3 + \frac{\sqrt{15}}{15} qu^3 v^5 + \frac{\sqrt{2}}{6} qu^3 v^6 + \frac{3}{8} qu^4 v^4 + \frac{\sqrt{5}}{5} qu^4 v^5 + \frac{\sqrt{6}}{12} qu^4 v^6 + \frac{1}{10} q(3l - 8)u^5 v^5 + \frac{\sqrt{30}}{30} q(2l - 8)u^5 v^6 , \)

\( J S^{1/2}_u S^{1/2}_v M_{B_{α}NT_{4q}} (u, v) = \frac{1}{6} qu^9 + \frac{1}{120} ( 45 + 8 \sqrt{15} ) qu^8 + \frac{1}{30} ( 5\sqrt{2} + 6 \sqrt{5} ) qu^9 + \frac{\sqrt{6}}{12} qu^{10} + \frac{1}{10} q(3l - 8)u^{10} + \frac{\sqrt{30}}{30} q(2l - 8)u^{11} \)

\( D_u J S^{1/2}_u S^{1/2}_v M_{B_{α}NT_{4q}} (u, v) = qu^6 + \frac{1}{15} ( 45 + 8 \sqrt{15} ) qu^8 + \frac{3}{10} ( 5\sqrt{2} + 6 \sqrt{5} ) qu^9 + \frac{5\sqrt{6}}{6} qu^{10} + q(3l - 8)u^{10} + \frac{11\sqrt{30}}{30} q(2l - 8)u^{11} \)

\( \frac{1}{2} D_u J S^{1/2}_u S^{1/2}_v M_{B_{α}NT_{4q}} (u, v) = \frac{1}{2} qu^6 + \frac{1}{30} ( 45 + 8 \sqrt{15} ) qu^8 + \frac{3}{20} ( 5\sqrt{2} + 6 \sqrt{5} ) qu^9 + \frac{5\sqrt{6}}{12} qu^{10} + \frac{1}{2} q(3l - 8)u^{10} + \frac{11\sqrt{30}}{60} q(2l - 8)u^{11} , \)
\[ D_u M_{B_N, NT_{u}} (u, v) = \frac{3}{2} qu^3 v^3 + 3qu^3 v^5 + 3qu^3 v^6 + 6qu^4 v^4 + 8qu^4 v^5 + 4qu^4 v^6 + \frac{5}{2} q(3l - 8)u^5 v^5 + 5q(2l - 8)u^5 v^6, \]
\[ D_v M_{B_N, NT_{u}} (u, v) = \frac{3}{2} qu^3 v^3 + 5qu^3 v^5 + 6qu^3 v^6 + 6qu^4 v^4 + 10qu^4 v^5 + 6qu^4 v^6 + \frac{5}{2} q(3l - 8)u^5 v^5 + 6q(2l - 8)u^5 v^6, \]
\[ (D_u + D_v) M_{B_N, NT_{u}} (u, v) = 3qu^3 v^3 + 8qu^3 v^5 + 9qu^3 v^6 + 12qu^4 v^4 + 18qu^4 v^5 + 10qu^4 v^6 + 5q(3l - 8)u^5 v^5 + 11q(2l - 8)u^5 v^6, \]
\[ \frac{1}{2} (D_u + D_v) M_{B_N, NT_{u}} (u, v) = \frac{3}{2} qu^3 v^3 + 4qu^3 v^5 + \frac{9}{2} qu^3 v^6 + 6qu^4 v^4 + 9qu^4 v^5 + 5qu^4 v^6 + \frac{5}{2} q(3l - 8)u^5 v^5 + \frac{11}{2} q(2l - 8)u^5 v^6, \]
\[ D_u D_v M_{B_N, NT_{u}} (u, v) = \frac{9}{2} qu^3 v^3 + 15qu^3 v^5 + 18qu^3 v^6 + 24qu^4 v^4 + 40qu^4 v^5 + 24qu^4 v^6 + \frac{25}{2} q(3l - 8)u^5 v^5 + 30q(2l - 8)u^5 v^6, \]
\[ \frac{1}{2} (D_u D_v) M_{B_N, NT_{u}} (u, v) = \frac{9}{4} qu^3 v^3 + \frac{15}{2} qu^3 v^5 + 9qu^4 v^4 + 12qu^4 v^5 + \frac{15}{2} qu^4 v^6 + 25q(3l - 8)u^5 v^5 + 15q(2l - 8)u^5 v^6, \]
\[ J M_{B_N, NT_{u}} (u, v) = \frac{9}{2} qu^4 + \frac{5}{2} qu^6 + 3qu^7 + \frac{9}{2} (3l - 6)u^10 + q(2l - 8)u^{11}, \]
\[ D_u^2 J M_{B_N, NT_{u}} (u, v) = 18qu^6 + 160qu^8 + 243qu^9 + 50q(3l - 6)u^{10} + 121q(2l - 8)u^{11}, \]
\[ \frac{1}{4} D_u^3 J M_{B_N, NT_{u}} (u, v) = \frac{9}{2} qu^5 + 40qu^7 + \frac{243}{4} qu^9 + \frac{25}{2} q(3l - 6)u^{10} + \frac{121}{4} q(2l - 8)u^{11}, \]
\[ Q_u (-2) J M_{B_N, NT_{u}} (u, v) = \frac{9}{2} qu^4 + \frac{5}{2} qu^6 + 3qu^7 + \frac{9}{2} (3l - 6)u^8 + q(2l - 8)u^9, \]
\[ D_u^2 Q_u (-2) J M_{B_N, NT_{u}} (u, v) = 8qu^5 + 90qu^7 + 147qu^9 + 32q(3l - 6)u^8 + 81q(2l - 8)u^9, \]
\[ \chi_1^u J M_{B_N, NT_{u}} (u, v) = \frac{\sqrt{6}}{12} qu^6 + \frac{5\sqrt{5}}{8} qu^8 + qu^9 + \frac{3\sqrt{10}}{10} q(3l - 6)u^{10} + \frac{\sqrt{11}}{11} q(2l - 8)u^{11}, \]
\[ D_u^3 J M_{B_N, NT_{u}} (u, v) = \frac{6}{2} qu^5 + \frac{5\cdot 8}{2} qu^7 + 3\cdot 9 qu^9 + \frac{10}{2} q(3l - 6)u^{10} + 11^3 q(2l - 8)u^{11}, \]
\[ D_v (D_u + D_v) M_{B_N, NT_{u}} (u, v) = 9qu^6 + 40qu^8 + 54qu^9 + 48qu^4 v^4 + 90qu^4 v^5 + 60qu^4 v^6 + 25(3l - 8)u^5 v^5 + 66q(2l - 8)u^5 v^6, \]
\[ D_u D_v (D_u + D_v) M_{B_N, NT_{u}} (u, v) = 27qu^6 + 120qu^8 + 162qu^9 + 192qu^4 v^4 + 360qu^4 v^5 + 240qu^4 v^6 + 125(3l - 8)u^5 v^5 + 330q(2l - 8)u^5 v^6. \]
We studied the important nanotube known as boron α-nanotube by computing their M-polynomial and then recovered some important degree-based TIs. The graphical representations of the results are presented.

4. Conclusion
in Figure 3. The results obtained will be useful in helping to solve many problems in the field of chemical analysis.

Data Availability

No data were used to support this research.

Conflicts of Interest

The author(s) declare that there are no conflicts of interest regarding the publication of this paper.

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