Better Termination for Prolog with Constraints

Markus Triska\textsuperscript{1}, Ulrich Neumerkel\textsuperscript{1}, and Jan Wielemaker\textsuperscript{2}

\textsuperscript{1} Technische Universität Wien, Austria
\{triska,ulrich\}@complang.tuwien.ac.at
\textsuperscript{2} Universiteit van Amsterdam, The Netherlands
J.Wielemaker@uva.nl

Abstract. Termination properties of actual Prolog systems with constraints are fragile and difficult to analyse. The lack of the occurs-check, moded and overloaded arithmetical evaluation via \texttt{is/2} and the occasional nontermination of finite domain constraints are all sources for invalidating termination results obtained by current termination analysers that rely on idealized assumptions. In this paper, we present solutions to address these problems on the level of the underlying Prolog system. Improved unification modes meet the requirements of norm based analysers by offering dynamic occurs-check detection. A generalized finite domain solver overcomes the shortcomings of conventional arithmetic without significant runtime overhead. The solver offers unbounded domains, yet propagation always terminates. Our work improves Prolog’s termination and makes Prolog a more reliable target for termination and type analysis. It is part of SWI-Prolog since version 5.6.50.

1 Introduction

Termination plays a central role in Prolog programs. Prolog’s complex control mechanism often taxes a programmer’s intuition about termination. Tools to support both experts and beginners are therefore highly valuable and the development of such systems has received considerable attention \cite{8,4,12}. One of the authors was particularly interested in developing termination tools for supporting beginners within the learning environment GUPU \cite{14}. In a collaborative effort, the termination inference system cTI \cite{12} was developed that featured not only a web interface but was designed to specifically meet the incremental demands for an on-the-fly analyser by employing a strict bottom up approach.

Much to our chagrin, the resulting system soon showed the limitations of current approaches for our original goals. cTI worked quite impressively for current benchmarks but did not reflect the entire spectrum of termination properties of actual Prolog implementations. cTI—like most other norm based approaches \cite{4}— was founded on some assumptions that are not true for existing Prolog systems. As a consequence, the termination conditions inferred with cTI are not literally applicable to the target system—at that time SICStus Prolog. We note that these problems do not show in existing termination benchmarks, but are frequently occurring in the incorrect programs beginners write. The source of
the problem is the lack of the occurs-check in existing Prolog implementations giving way to rational trees that can no longer be mapped onto the integers. While there are approaches to determine occurs-check freeness statically [6], as well as finite trees [2] we finally chose to go for the maximum which is performing the occurs-check dynamically.

With the addition of constraints to Prolog’s core language, new sources of unforeseen nontermination opened, further complicating procedural reasoning. The traditional \texttt{is/2} predicate with its overloaded semantics posed even more problems. To meet all these needs we implemented a new version of a generalized finite domain solver. This library subsumes the functionality of integer arithmetic and constraint programming, combines their strengths, and terminates always, permitting better termination results.

\textit{Content.} We first describe our new approach to the old occurs-check problem and then discuss our improvement to \texttt{clpfd} to subsume \texttt{is/2}-functionality. Finally we present our new always terminating implementation of \texttt{clpfd}.

2 \ Occurs-check

Most existing Prolog implementations use rational tree unification [5] to avoid overheads caused by the occurs-check of finite tree unification. While rational trees are an interesting domain in their own right, they are often an indication for programming errors. For beginners, it is very common to accidentally confuse assignment and unification. Goals like \texttt{Xs = [X|Xs]} are often written with the intention to add to the list \texttt{Xs} an element. Also misunderstandings concerning the scoping of variables lead to infinite terms. Exactly such cases are not covered by existing norm based approaches that assume the finiteness of terms.

We added two new standard conforming unification modes that prevent the creation of infinite terms. Apart from traditional occurs-check that fails silently, a new mode was added to better localize attempts to create infinite terms. By issuing \texttt{?- set_prolog_flag(occurs_check,error)}. at runtime all attempts to create infinite terms are detected and an error is issued. In this manner all programs are identified that create infinite terms. Also, most programs subject to occurs-check (STO) are detected, that are ruled out by the ISO standard [10].

Our implementation tries to avoid the costly occurs-check scan for the most frequent cases of passing variables. Current Prolog implementations allocate variables that do not occur within a structure in a separate storage area, mostly known as the goal or environment stack. Those variables are unified in constant time with structured terms, as the cannot be the subterm of a structure. In this manner most uses of difference lists and differences with other data structures do not require the occurs-check. The actual testing can be further reduced taking into account that Prolog compilers emit specialised unification instructions where possible, based on its knowledge about the arguments involved in the unification. Only the cases of instructions of general unification are subject to occurs check. All other cases do not involve any overhead. As of version 5.7, all
overheads for handling the list differences of DCGs are completely removed for an initial goal \texttt{phrase/2}. For \texttt{phrase/3} there is a single occurs-check for each solution found.

3 Overcoming \texttt{is/2}

Using \texttt{is/2} in pure programs has many disadvantages. For one, \texttt{is/2} works only for certain restricted modes thereby limiting the relational view of a predicate. This relational view permits to test programs more extensively—testing them with generalized modes. Even if those generalized modes are not used in the final application, they help to detect otherwise undiscovered problems. Consider for example McCarthy’s “mysterious” 91-function. With the following query we search for results different to 91.

\begin{verbatim}
mc_carthy_91(X, Y) :-
    X #> 100, Y #= X - 10.
mc_carthy_91(X, Y) :-
    X #=< 100, Z #= X + 11,
    mc_carthy_91(Z, Z1),
    mc_carthy_91(Z1, Y).
\end{verbatim}

?- \texttt{Y \#\#= 91, mc_carthy_91(X, Y)}.
\texttt{Y in 92..sup,}
\texttt{-10+X\#=Y,}
\texttt{X in 102..sup ;}
(\texttt{looping})

Attempts to emulate with \texttt{is/2} different modes require the explicit usage of \texttt{var/1} and \texttt{nonvar/1}, two built-ins that lead frequently to errors due to forgotten modes.

The overloading of integer and floating-point arithmetic is another source of frequent errors with \texttt{is/2}. An accidentally introduced float might lead to unexpected failures. Modeling without knowing whether or not a variable is a float is not reliably possible, thereby weakening termination analysis [8].

For these reasons we propose to use in place of \texttt{is/2} the corresponding \texttt{#=/2} of \texttt{clpfd} and the corresponding comparison relations. To make this shift more practical we removed the common limits of \texttt{#=/2} to small integers and improved execution for such simple moded cases. While using \texttt{#=/2} in place of \texttt{is/2} incurred overheads greater than two orders of magnitude for small loops, our improved implementation is only about 30\% slower than naive \texttt{is/2}. In this manner, we obtain predicates that are simpler to type and that are not moded.

The original version of \texttt{factorial/2} is not tail recursive due to the modedness of \texttt{is/2}. The space for allocating the environments in the original version is traded for allocating constraints on the global stack. \texttt{factorial/2} now terminates if either the first argument is finite, or the second argument is finite and not equal zero.
factorial(0, 1).
factorial(N, F) :-
    N #> 0,
    F #= F0*N,
    N1 #= N - 1,
    factorial(N1, F0).

?- Y in 1..5, factorial(X,Y).
Y = 1, X = 0 ;
Y = 1, X = 1 ;
Y = 2, X = 2 ;
false.

4 Terminating constraints

Current implementations of finite domain constraints are optimized for the traditional usage pattern of constraint satisfaction. First, variables get their associated domains, then the constraints between variables are posted, and finally labeling searches for actual solutions. In current implementations, the declaration of a variable’s domain is just a simple goal. (Original systems required a static declaration.) The extension from this limited view toward a general constraint systems over integers, a kind of CLP(Z), is straightforward.

By accepting variables without a finite domain, we open the door to nonterminating constraint propagation. Consider the query ?- X#>Y, Y#>X, X#>0. Existing constraint solvers will try to reduce the domains until the maximal domain value is encountered, then failing or yielding a representation error. We therefore consider this case the same as genuine nontermination. Note that nontermination does not only occur due to posting a constraint but also may happen during labeling.

?- X#>Y, Y#>X, X#>B*Y, B in -1..0, labeling([],[B])

Termination within constraint propagation is ensured by propagating domain changes in infinite domains only once. At the price of weakening consistency we can now guarantee that clpfd and all unifications with constrained variables terminate.

4.1 Observing termination

The notion of termination and nontermination are idealizations of actual observable behavior that lead to seemingly paradoxical situations. The query ?- X#>X*X. terminates rapidly in SICStus 3 with a representation error. Still, we consider this a case of non-termination. For ?- abs(X)#<7^7^7,X#>Y,Y#>X. in SWI,
termination is not observable within reasonable time. However, we consider this case terminating.

Another rather unintuitive consequence concerns the termination property of the entire program. While our improvement guarantees termination for unification and all clpfd-goals, and therefore might improve termination of the entire program, there are cases where a stronger propagation that does not terminate in the general case will nevertheless result in better termination of the entire program. This may happen, if the stronger propagation results in failure preventing an infinite loop, while terminating propagation yields inconsistency.

4.2 Ad hoc termination proofs

With an always terminating clpfd, we are able to perform some simple forms of termination testing when using labeling. One frequent problem with larger constraint problems concerns the time span to wait for the first solution. Quite often labeling is considered to be inefficient, when in reality the actual predicate definition that posts the constraints does not terminate. To avoid this situation we separate the actual relation from labeling. In place of the original predicate $p/n$ we define a new relation $p_/n+1$ (“core relation”) that contains an additional argument for the list of variables to be labeled. Consider for example as original query $?- \text{queens}(Ds)$, describing solutions for a given fixed length of $Ds$. This query is now formulated as $?- \text{queens_}(Ds,Zs), \text{labeling}([],Zs)$. Suppose now that the answer does not appear immediately. Should we wait for an answer? What, if the query does not terminate? To better understand the termination properties involved we can consider the following query. If $?- \text{queens_}(Ds,Zs), \text{false}.$ terminates (by observation), we know also that the query followed by labeling will terminate, since in our implementation labeling/2 is guaranteed to terminate. We thus obtain a proof for termination by observing the termination of another related predicate. In systems without our favorable termination property, a terminating $?- \text{queens_}(Ds,Zs), \text{false}.$ does not constitute a termination proof of the goal followed by a search with labeling/2.

4.3 Black-box testing

While developing and testing library(clpfd), it soon became evident that manual testing and testing with given applications is not sufficient. We noted as one of the most prominent coding errors the omission of certain rare cases of instantiations. The current implementation in Prolog based on hProlog-style attributed variables [7] does not guarantee any properties concerning the correctness of the implementation. The concerns consistency and correctness must be dealt with on the same level - thereby increasing the chance for errors. As one of the authors experienced similar problems with other constraint implementations prior to SWI, it was evident that a more systematic approach was needed. Existing approaches to testing and specifying finite domain constraints [1] were also not very attractive, as they require considerable effort for specifying the actual propagation mechanism. Such complex specifications may again be a further source
of errors. We therefore focused on testing with strictly minimal information - thereby minimizing demotivating cases of false alarms.

We concentrated on testing a fixed set of algebraic properties for small finite domains. So far, all encountered correctness errors could be shown to violate those properties. We illustrate our approach with an error located in this manner (i3a#98). The query ?- X in 0..2, 0/X#=0. should succeed, but failed. Even to the experienced constraint programmer it is not obvious by naively inspecting this query what the correct result should be. The bug was located automatically by detecting a difference between the following two queries:

?- X in 0..2, 0/X #= 0, X = 1.
?- X = 1, X in 0..2, 0/X #= 0.

The first query failed, the second succeeded. Evidently, there must be at least one error—either in the first or second query, or in both. Most errors found are related to the implementation of nonlinear constraints like general multiplication. Also, sharing of variables was a frequent cause for errors. In total, more than 30 errors of this kind were found by systematically exploring a tiny slice of all possible formulae.

For efficient testing, (rapid) termination of clpfd’s propagation is indispensable. This permits to test many queries simultaneously. On systems with nonterminating propagation, we would have to rely on timeout mechanisms to interrupt certain queries that cannot be tested in this way.

4.4 Related work

SICStus Prolog [3] was the first system to generalize finite domain constraints without sacrificing correctness. It uses small integers for domains but signals domain overflows as representation errors and not as silent failures.

Built-in support for the occurs-check has been implemented with similar techniques in Sepia Prolog [13] and its successor Eclipse Prolog [16].

5 Conclusions

The presented improvements constitute a more solid target for termination analysis than prior implementations. We hope that they will lead to the development of more powerful analysers.

Acknowledgements. We would like to thank Philipp Kolmann of ZID for his generous support on the Condor based [15] WINZIG-grid [11] at TU Wien that we use to perform large scale tests.
References

1. K.R. Apt, P. Zoeteweij. An Analysis of Arithmetic Constraints on Integer Intervals, Constraints 12(4). 2007.
2. R. Bagnara, E. Zaffanella, R. Gori, P. Hill. Boolean functions for finite-tree dependencies. LPAR 2001.
3. M. Carlsson, G. Ottosson, B. Carlson. An Open-Ended Finite Domain Constraint Solver. PLILP. 1997.
4. M. Codish, C. Taboch. A Semantic Basis for the Termination Analysis of Logic Programs. JLP. 41(1), 1999.
5. A. Colmerauer. Prolog and Infinite Trees. Logic Programming, K.L. Clark, S.-A. Tärnlund (eds), 1982.
6. L. Crnogorac, A. Kelly, H. Søndergaard. A comparison of three occur-check analysers. SAS 1996.
7. B. Demoen. Dynamic attributes, their hProlog implementation, and a first evaluation, TR CW 350, Leuven, 2002.
8. N. Dershowitz, N. Lindenstrauss, Y. Sagiv, A. Serebrenik. Automatic Termination Analysis of Programs Containing Arithmetic Predicates. Electr. Notes TCI 30(1), 1999.
9. A. Faustino da Silva, V. S. Costa. The Design and Implementation of the YAP Compiler, ICLP 2006.
10. ISO/IEC 13211-1 Programming languages - Prolog - Part 1: General core. 1995. (7.3 Unification)
11. Ph. Kolmann. University Campus Grid Computing. Diploma thesis, TU Wien, 2005.
12. F. Mesnard, U. Neumerkel. Applying Static Analysis Techniques for Inferring Termination Conditions of Logic Programs. SAS 2001.
13. M. Meier. SEPIA: A Basis for Prolog Extensions. LPAR 1992.
14. U. Neumerkel, St. Kral. Declarative program development in Prolog with GUPU. WLPE. 2002.
15. D. Thain, T. Tannenbaum, M. Livny. Condor and the Grid. In F. Berman, G. Fox, A. Hey (ed.), Grid Computing: Making the Global Infrastructure a Reality. Wiley, 2003.
16. M. Wallace, St. Novello, J. Schimpf. ECLiPSe: A Platform for Constraint Logic Programming, ICL systems journal 1997.
17. J. Wielemaker. An Overview of the SWI-Prolog Programming Environment, WLPE 2003.