Research on cogging torque optimization design of permanent magnet synchronous wind turbine

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Abstract. Cogging torque is one of the unique problems of permanent magnet generators. Its main cause is the uneven distribution of the generator's magnetic permeability, which directly affects the starting and running performance of the generator. The study of cogging torque suppression methods is of great significance for improving the operating stability and service life of generators. Through the analysis of the principle of cogging torque, an optimization method for the amplitude of cogging torque based on Taguchi algorithm for the two parameters of pole arc coefficient and skew angle is established. And the finite element analysis method is used to quantitatively compare the characteristic parameters of the generator model before and after the optimization by Taguchi algorithm. The results show that when the pole arc coefficient and the angle of the chute are in the optimal value at the same time, the cogging torque of the generator can be greatly reduced, and its air gap magnetic density waveform and induced electromotive force waveform are ideal, which provides a research method for the design and parameter optimization of large megawatt permanent magnet synchronous wind turbines.

1 Introduction

Permanent magnet synchronous motors are widely used in the research and development of wind power generators. Compared with excitation generators, they have the advantages of high torque-to-current ratio, high torque-to-volume ratio, high efficiency, small size and simpler structure. Due to the existence of the stator core slot of the permanent magnet synchronous generator, the interaction between the stator teeth and the magnetic steel during the operation of the generator will cause the change of the magnetic field, which will lead to the torque pulsation caused by the cogging torque [1]. It will cause unnecessary vibration and noise of the generator, and even reduce its dynamic performance to a certain extent. Therefore, the influence of cogging torque on the performance of the generator must be considered in the design process of permanent magnet wind turbines [2].

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There are many factors that affect the magnitude of the cogging torque, such as the stator and rotor materials, different permanent magnet materials and structures. In engineering, the cogging torque is mainly suppressed by changing the structure design of the generator body. Literature [3] ~ [6] studied the influence of the optimal combination of stator cogging parameters, armature slot width and pole arc coefficient on cogging torque; Literature [7] studied the influence of surface auxiliary grooves on cogging torque, and calculated the number of auxiliary grooves by multi-objective genetic algorithm; Literature [8] studied the influence of cogging torque on noise; Literature [9]~[15] carried out research and simulation work on cogging torque suppression methods; In the optimization algorithm of cogging torque, literature [16] uses genetic algorithm to optimize the cogging torque of the external rotor motor; Literature [17] optimized the cogging torque of low-speed permanent magnet motors based on the RBF approximation model; Literature [18] ~ [20] used Taguchi algorithm to optimize the structural parameters of permanent magnet synchronous motors.

In this paper, two models of 10 MW permanent magnet synchronous wind turbine are designed based on the research of cogging torque. Based on Taguchi algorithm, the cogging torque of the two motors is optimized by two optimization factors: the pole arc coefficient and the inclined slot angle. After determining the best combination plan, compare the cogging torque under a variety of pole arc coefficients and skew angle assembly plans, and analyze the influence of the cogging torque on the performance of the generator. The effectiveness of the method is verified by the simulation test of two generator design schemes.

2 Analysis of cogging torque generation mechanism of permanent magnet generator

2.1 Generation mechanism of cogging torque

In the process of generator design, the problem of cogging torque is always an unsolved problem. The energy method is usually used to calculate cogging torque. Because the difference of permeance between the stator teeth and the segmented permanent magnet is small, the magnetic field around the stator teeth basically remains unchanged. However, the permeance of the stator teeth between the permanent magnets in the two adjacent magnetic sleeves will change, which will cause the change of energy stored in the magnetic field of the motor. The method of calculating the cogging torque usually uses the energy method. The magnetic permeability between the stator teeth and the segmented permanent magnets changes very little, so the magnetic field around the stator teeth remains basically unchanged. However, the magnetic permeance of the stator tooth area between the permanent magnets in two adjacent magnetic sleeves changes, which will cause the change of the stored energy of the motor magnetic field and generate cogging torque $T_{\text{cog}}(\alpha)$. The calculation formula is:

$$T_{\text{cog}}(\alpha) = \frac{\partial W}{\partial \alpha} \tag{1}$$

Where $\alpha$ is the angle between the centerline of the stator teeth and the centerline of the permanent magnet. Without considering the saturation of the magnetic field, the energy stored in the magnetic field of the motor can be approximately regarded as the energy in the
air gap between the armature tooth and the permanent magnet. The stored energy of the magnetic field of the motor can be expressed as:

\[ W \approx W_{\text{airgap+PM}} = \frac{1}{2\mu_0} \int B^2 dV \]  

(2)

Where \( W_{\text{airgap+PM}} \) is the energy in the air gap between the armature tooth and the permanent magnet. \( \mu_0 \) is the permeability of air. \( B \) is the magnetic induction intensity. \( V \) is the air gap volume between the armature tooth and the permanent magnet.

The air gap flux density between the stator teeth and the permanent magnets along the surface of the permanent magnet synchronous motor stator armature can be approximately expressed as:

\[ B(\theta, \alpha) = B_r(\theta) \frac{h_m(\theta)}{h_m(\theta) + \delta(\theta, \alpha)} \]  

(3)

Where \( \theta \) is the angle between the permanent magnet and the rotor shaft when it moves in the circumferential direction. \( h_m(\theta) \) is the thickness of the permanent magnet pole. \( B_r(\theta) \) is the remanence of permanent magnets. \( \delta(\theta, \alpha) \) is the distribution coefficient of the effective air gap length of the permanent magnet along the circumferential direction;

Substituting formula (3) into formula (2), the stored energy of the motor's magnetic field is obtained:

\[ W = \frac{1}{2\mu_0} \int B_r^2(\theta) \left( \frac{h_m(\theta)}{h_m(\theta) + \delta(\theta, \alpha)} \right)^2 dV \]  

(4)

Assuming that the magnetic flux of each stage of the generator is constant, expand A through Fourier transform to get the following formula:

\[ B_r^2(\theta) = B_{s0} + B_{sN} \cos(2np\theta) \]  

(5)

Where: \( B_{sn} \) is the \( N \)-th Fourier expansion coefficient of \( A \); \( p \) is the number of generator pole pairs. that is:

\[ \xi(\theta, \alpha) = \frac{h}{h + g(\theta, \alpha)} \]  

(6)

Fourier decomposition of A:

\[ \xi^2(\theta, \alpha) = \xi_{s0} + \sum_{n=1}^{\infty} \xi_{sn} \cos(Nz(\theta + \alpha)) \]  

(7)

Where: \( \xi_{sn} \) is the \( N \)-th Fourier expansion coefficient of \( \xi^2(\theta, \alpha) \). From this, the general expression of cogging torque can be obtained as:

\[ T_c = \frac{L_{sf} N_s \pi}{4\mu_0} (R_2^2 - R_1^2) \sum_{n=1}^{\infty} \frac{\xi_{sn}}{z_p} B_{sN} \sin(nN_s \alpha) \]  

(8)
Where: $L_a$ is the axial length of the generator; $N_s$ is the number of generator slots; $R_1$ is the inner radius of the air gap; $R_2$ is the outer radius of the air gap;

It can be seen that both $B^2_r(\theta)$ and $\xi^2(\theta,\alpha)$ are the influencing factors of the amplitude of the cogging torque and the waveform. But not all the Fourier expansion series have an effect on the cogging torque waveform. For $B^2_r(\theta)$, only the $N_s/2p$ expansion series have an effect. For $\xi^2(\theta,\alpha)$, only the $n$-th Fourier expansion series has an effect on the cogging torque, so if $B^2_r(\theta)$ and $\xi^2(\theta,\alpha)$ can be reduced as much as possible, the cogging torque can be effectively suppressed.

For a permanent magnet generator with the same magnetic pole shape and size and the same effect, the expression of the number of cycles $N_p$ of the cogging torque within a tooth pitch is:

$$N_p = \frac{2p}{\text{GCD}(2p, Q)}$$  \hspace{1cm} (9)

Among them, GCD $(2p, Q)$ is the greatest common divisor of the number of slot poles.

### 2.2 Introduction to Taguchi’s algorithm mechanism and optimization process

Taguchi algorithm is an experimental method developed by Dr. Genichi Taguchi of Japan. It is a low-cost and high-efficiency quality engineering calculation method based on the idea of local optimization. The optimization flow chart is as follows:

![Optimization flow of Taguchi Algorithm.](image)

**Fig. 1.** Optimization flow of Taguchi Algorithm.

### 2.3 Selection of optimization goals and optimization factors

Taguchi method can achieve multi-objective optimization. The optimization target is the dependent variable in the experiment, and the optimization factor is the independent variable in the experiment. In the work of this article for the design of generators, two indexes of motor efficiency and cogging torque are selected as optimization targets. In the process of selecting the optimization factor, the parameters that have a more obvious impact on the optimization goal should be selected. In addition, by skewing the stator, the unfavorable factors such as the harmonic amplitude in the air gap magnetic density...
waveform can be reduced to reduce the cogging torque. Therefore, the angle of the stator skewer is also used as an optimization factor.

2.4 Determine the optimal range and level of optimization factors

Through the traditional generator design method and the RMxprt module, the above two optimization factors are parameterized, and the performance of the optimization target under different parameter factors is obtained. According to different performances, determine the optimal range of optimization factors, divide the optimization factors into 3–5 equidistantly, and name the level values of each optimization factor respectively in order.

2.5 Determine the optimal range and level of optimization factors

Orthogonal experiment can optimize the level of multiple factors, has the important characteristics of being scattered, neat and comparable, and can greatly reduce the number of experiments and save the cost of experiments. Orthogonal table can generally be expressed as $L_{n}(A^{k})$, where: represents the number of experiments; $A$ represents the number of level values; $k$ represents the number of optimization factors. The finite element simulation experiment was carried out according to the orthogonal table, and the optimized target value of the optimized silver under different combinations was obtained.

2.6 Analysis of the mean and variance

In order to analyze the influence of the change of the optimization factor on each performance index of the motor, and the proportion of the influence, the average value of the optimization factor at different levels must be analyzed first. For example, the average value of the cogging torque of the integer slot scheme when the pole arc coefficient is level A1 is:

$$T_{cog}(\alpha_{p1}) = \frac{1}{4}(T_{cog}(1) + T_{cog}(2) + T_{cog}(3) + T_{cog}(4) + T_{cog}(5))$$  \hspace{1cm} (10)

Where: $T_{cog}(\alpha_{p1})$ is the cogging torque at level 1 for the optimization factor polar arc coefficient. $T_{cog}(1), T_{cog}(2), T_{cog}(3), T_{cog}(4), T_{cog}(5)$ are respectively the cogging torque in the first 1, 2, 3, 4, and 5 tests.

In the same way, the average value of generator performance indicators at different levels of other optimization factors can be calculated.

In the analysis of variance, we must first calculate the overall average (SS) of each performance index. Secondly, calculate the variance (SSF), the formula is as follows:

$$SS = \frac{1}{50} \sum_{i=1}^{50} T_{cog}(i)$$  \hspace{1cm} (11)

$$SSF(T_{cog}) = \frac{1}{\lambda} \sum_{i=1}^{\lambda} (T_{cog}(i) - SS(T_{cog}))^2$$  \hspace{1cm} (12)
Where: \( SS(T_{\text{cog}}) \) is the average value of the cogging torque; \( T_{\text{cog}}(i) \) is the cogging torque in the i-th test; \( SSF(T_{\text{cog}}) \) is the variance value of the cogging torque of the generator, and \( \lambda \) is the level number of each parameter.

In the same way, the motor performance variance and proportion of each optimization factor at 5 levels can be calculated, and the best combination of optimization factors can be determined according to the variance calculation results.

3 Taguchi algorithm optimization process

3.1 Determination of optimization factors and optimization goals

For two permanent magnet synchronous generators, the respective motor efficiency \( \eta \) and cogging torque \( T_{\text{cog}} \) are selected as the optimization targets. Select the respective pole arc coefficient \( \alpha_p \) and skew angle \( \text{Skew}_\theta \) as the optimization factor.

3.2 Determination of preferred range and level value

Because the two prototypes have the same capacity and similar structure, they are both built-in synchronous wind turbines. Therefore, for the convenience of calculation, the same optimization range is selected for the two optimization factors. The design parameters of the two prototypes are given in Table 1 ~ 2, and the selection range of optimization factors is determined, as shown in Table 3. The range of optimization factors is divided into 5 parts, and the level values of integer slot scheme are named A1, A2, A3, A4 and A5 from small to large; the level values of fractional slot scheme are named B1, B2, B3, B4 and B5 from small to large, as shown in Table 4.

| Parameters                  | Value   | Parameters                  | Value   |
|-----------------------------|---------|-----------------------------|---------|
| Generator power             | 10750 kW| Core length                 | 750 mm  |
| Pole of Pairs               | 9       | Minimum air gap width       | 4 mm    |
| Number of stator slots      | 216     | Generator speed             | 325 rpm |

Table 1. Main parameters of integer slot scheme.

| Parameters                  | Value   | Parameters                  | Value   |
|-----------------------------|---------|-----------------------------|---------|
| Generator power             | 10750 kW| Core length                 | 700 mm  |
| Pole of Pairs               | 12      | Minimum air gap width       | 4 mm    |
| Number of stator slots      | 180     | Generator speed             | 315.4 rpm|

Table 2. Main parameters of fractional slot scheme.

| Optimization factor       | Preferred range |
|---------------------------|-----------------|
| Polar arc coefficient     | 0.65–0.85       |
| Skew angle / slot         | 0–1             |

Table 3. Selection range of optimization factors.
Table 4. Optimization factor levels.

| Horizontal factor | A1 (B1) | A2 (B2) | A3 (B3) | A4 (B4) | A5 (B5) |
|-------------------|---------|---------|---------|---------|---------|
| Polar arc coefficient | 0.65 | 0.7 | 0.75 | 0.8 | 0.85 |
| Skew angle / slot | 0 | 0.25 | 0.5 | 0.75 | 1 |

3.3 Establishment of orthogonal experiment

According to table 4 and the construction principle of orthogonal table to establish orthogonal table. The finite element method is used to establish the corresponding number of motor models, and the experimental results are shown in Table 5. According to the experimental results, the average values of cogging torque and motor efficiency under different levels of optimization factors are calculated. The calculation results are shown in Table 6. According to the formula (12), the variance and its proportion of the optimization factor under the corresponding performance index can be calculated, as shown in Table 7.

Table 5. Orthogonal Table and Finite Element Results.

| No. | Experimental matrix |  Tcog | η  | No. | Experimental matrix |  Tcog | η  | No. | Experimental matrix |  Tcog | η  |
|-----|--------------------|-------|---|-----|--------------------|-------|---|-----|--------------------|-------|---|
| 1   | A1 A1              | 1.285 | 98.44 | 18  | A4 A3              | 0.784 | 98.19 | 35  | B2 B5              | 0.518 | 98.39 |
| 2   | A1 A2              | 0.864 | 98.43 | 19  | A4 A4              | 0.653 | 98.30 | 36  | B3 B1              | 0.902 | 97.84 |
| 3   | A1 A3              | 0.824 | 98.44 | 20  | A4 A5              | 0.533 | 98.34 | 37  | B3 B2              | 0.604 | 98.24 |
| 4   | A1 A4              | 0.854 | 98.08 | 21  | A5 A1              | 0.696 | 98.30 | 38  | B3 B3              | 0.282 | 97.85 |
| 5   | A1 A5              | 0.875 | 97.81 | 22  | A5 A2              | 0.574 | 97.97 | 39  | B3 B4              | 0.255 | 97.97 |
| 6   | A2 A1              | 1.172 | 97.98 | 23  | A5 A3              | 0.538 | 98.39 | 40  | B3 B5              | 0.104 | 98.19 |
| 7   | A2 A2              | 0.843 | 98.14 | 24  | A5 A4              | 0.527 | 98.28 | 41  | B4 B1              | 0.937 | 98.48 |
| 8   | A2 A3              | 0.792 | 98.49 | 25  | A5 A5              | 0.519 | 97.83 | 42  | B4 B2              | 0.809 | 97.96 |
| 9   | A2 A4              | 0.637 | 98.11 | 26  | B1 B1              | 1.671 | 98.01 | 43  | B4 B3              | 0.784 | 98.11 |
| 10  | A2 A5              | 0.564 | 98.08 | 27  | B1 B2              | 1.301 | 97.93 | 44  | B4 B4              | 0.664 | 98.24 |
| 11  | A3 A1              | 1.036 | 98.30 | 28  | B1 B3              | 1.161 | 98.23 | 45  | B4 B5              | 0.467 | 98.48 |
| 12  | A3 A2              | 0.819 | 98.09 | 29  | B1 B4              | 0.831 | 98.42 | 46  | B5 B1              | 0.964 | 98.46 |
| 13  | A3 A3              | 0.795 | 97.82 | 30  | B1 B5              | 0.608 | 98.01 | 47  | B5 B2              | 0.774 | 98.39 |
| 14  | A3 A4              | 0.657 | 98.08 | 31  | B2 B1              | 0.916 | 97.92 | 48  | B5 B3              | 0.645 | 97.87 |
| 15  | A3 A5              | 0.542 | 97.89 | 32  | B2 B2              | 0.706 | 98.24 | 49  | B5 B4              | 0.484 | 97.86 |
| 16  | A4 A1              | 0.926 | 97.88 | 33  | B2 B3              | 0.675 | 97.89 | 50  | B5 B5              | 0.385 | 98.40 |
| 17  | A4 A2              | 0.806 | 98.01 | 34  | B2 B4              | 0.547 | 98.24 |     |                   |      |    |
Table 6. Average values of optimization factors under different levels.

| Design scheme         | Optimization factor | Horizontal value | cogging torque (kNm) | Efficiency  |
|-----------------------|---------------------|------------------|-----------------------|-------------|
| Integer slot scheme   | Polar arc coefficient | A1 0.940        | 98.24%                |
|                       |                     | A2 0.801        | 98.16%                |
|                       |                     | A3 0.769        | 98.04%                |
|                       |                     | A4 0.740        | 98.10%                |
|                       |                     | A5 0.570        | 98.15%                |
|                       | Skew angle / slot   | A1 1.023        | 98.18%                |
|                       |                     | A2 0.781        | 98.13%                |
|                       |                     | A3 0.746        | 98.27%                |
|                       |                     | A4 0.665        | 98.13%                |
|                       |                     | A5 0.606        | 97.99%                |
| Fractional slot       | Polar arc coefficient | B1 1.114        | 98.12%                |
| scheme                |                     | B2 0.672        | 98.14%                |
|                       |                     | B3 0.429        | 98.02%                |
|                       |                     | B4 0.732        | 98.25%                |
|                       |                     | B5 0.650        | 98.20%                |
|                       | Skew angle / slot   | B1 1.078        | 98.14%                |
|                       |                     | B2 0.839        | 98.15%                |
|                       |                     | B3 0.709        | 97.99%                |
|                       |                     | B4 0.556        | 98.15%                |
|                       |                     | B5 0.416        | 98.29%                |

Table 7. Variance and proportion of optimization factors under different performance indexes.

| Design scheme         | Optimization factor | Cogging torque $T_{cog}$ Value | Proportion | efficiency $\eta$ Value | Proportion |
|-----------------------|---------------------|-------------------------------|------------|-------------------------|------------|
| Integer slot scheme   | Polar arc coefficient | 0.014             | 41.17%        | 0.0045         | 36.00%     |
|                       | Skew angle          | 0.020             | 58.82%        | 0.0080         | 64.00%     |
|                       | total               | 0.034             | 100%          | 0.0125         | 100%       |
| Fractional slot       | Polar arc coefficient | 0.049             | 48.51%        | 0.0062         | 40.25%     |
| scheme                | Skew angle          | 0.052             | 51.49%        | 0.0092         | 59.75%     |
|                       | total               | 0.101             | 100%          | 0.0154         | 100%       |

According to the table, the combination of optimization factors with the smallest cogging torque and the highest efficiency for the integral slot solution with integral slot windings is $\alpha_p(A5)$ and $\text{Skew}_{(\phi)}(A5)$, that is, the optimal pole arc coefficient is 0.85, and the skew angle is 1 slot. The combination of optimization factors with the smallest cogging torque and the highest efficiency for the fractional slot concentrated winding with fractional slots is $\alpha_p(B3)$ and $\text{Skew}_{(\phi)}(B5)$. That is, the best pole arc coefficient is 0.75, and the chute angle is 1 slot. Therefore, the optimal combination of optimization factors has been determined, and then the finite element simulation verification work is carried out on the calculation results of the Taguchi method. That is, the best pole arc coefficient is 0.75, and the chute angle is 1 slot. Therefore, the optimal combination of optimization factors has
been determined, and then the finite element simulation verification work is carried out on the calculation results of the Taguchi method.

4 Simulation and verification of cogging torque of generator

In this paper, two megawatt permanent magnet synchronous generator prototypes are designed as calculation examples. The integral slot scheme adopts integral slot winding, and the fractional slot scheme adopts fractional slot concentrated winding. The two prototypes are modeled respectively, and the pole arc coefficient and armature structure determined by Taguchi method are simulated and verified by finite element analysis. The cross-sectional view cross sections of the two prototypes are shown in Fig 2.

![Cross-sectional view of finite element model](image)

**Fig. 2.** Sectional view of finite element model.

4.1 Selection of pole arc coefficient of magnetic steel

The pole arc coefficient in the built-in permanent magnet motor usually refers to the ratio of the pole arc length to the pole pitch. From the above analysis, it can be seen that the Fourier series expanded in the definition of cogging torque depends on the different number of slot poles.

According to the number of slot poles of the two prototypes, $B_r(\varphi_1(\theta))$ and $\xi^2(\theta,\alpha)$, which affect the cogging slot torque of the prototype, are respectively solved. The pole arc coefficient of one magnetic pole is taken as the independent variable to solve the pole arc coefficient of the other magnetic pole.

For the integer slot scheme, there are:

$$\frac{\xi_1 z_1}{2p_1} = \frac{216}{18} n_1$$

For the fractional slot scheme, there are:

$$\frac{\xi_2 z_2}{2p_2} = \frac{180}{24} n_2$$

Where, $\xi_1$ and $\xi_2$ are integers satisfying that $\frac{\xi z}{2p}$ is an integer.

From the above formula, it can be concluded that the Fourier series that affects the cogging torque of the integer slot scheme is $12k$ (k is an integer); the Fourier series that affects the cogging torque of the fractional slot scheme is $15k$ (k is an integer). The curves of $B_{rm}$ changing with polar arc coefficient of two prototypes are shown in Fig. 3 and Fig. 4.
It can be seen that the optimal polar arc coefficient of integer slot scheme is 0.85, and that of fractional slot scheme is 0.75, which is consistent with the results of Taguchi algorithm. The accuracy and reliability of the algorithm are further verified.

![Variation curve of Bm in integer slot scheme with pole arc coefficient.](image1)

**Fig. 3.** Variation curve of Bm in integer slot scheme with pole arc coefficient.

![Variation curve of Bm in fractional slot scheme with polar arc coefficient.](image2)

**Fig. 4.** Variation curve of Bm in fractional slot scheme with polar arc coefficient.

The parameter simulation of the polar arc coefficients of the two prototypes can be calculated based on the results of Taguchi algorithm. Among them, the curves 1-5 in Fig. 5 represent the waveform conditions when the pole arc coefficient is 0.65, 0.7, 0.75, 0.8 and 0.85, respectively.

The influence of polar arc coefficient on cogging torque is shown in Fig. 5. In integer slot scheme, when polar arc coefficient is 0.85, the cogging torque is smaller, which is 2.986kNm; In fractional slot scheme, when polar arc coefficient is 0.75, the waveform sinusoidal of cogging torque is better, and the amplitude is smaller, which is about 0.963kNm.

![Variation of cogging torque in integer slot scheme under different pole arc coefficients.](image3)

**Fig. 5- (a).** Variation of cogging torque in integer slot scheme under different pole arc coefficients.
Fig. 5-(b). Variation of cogging torque in fractional slot scheme under different pole arc coefficients.

Fig. 5. The influence of pole arc coefficient on cogging torque.

4.2 Selection of pole arc coefficient of magnetic steel

According to the conclusion of Taguchi algorithm, the pole arc coefficient of integer slot scheme is 0.85, and that of fractional slot scheme is 0.75. The change of cogging torque with the change of chute angle is observed.

In Fig. 6, it can be seen that the optimal skew angle of integer slot scheme with integral slot winding is 1 slot, and the cogging torque amplitude is about 500 nm; the optimal skew angle of fractional slot scheme with fractional slot concentrated winding is 1 slot, and the cogging torque amplitude is about 120 nm. It can be seen that the cogging torque can be reduced by 80% to 83% through the stator skewed slot winding. Under the same generator capacity, the cogging torque of using fractional-slot concentrated windings will be reduced by 90% to 94% compared to using integer-slot windings.

Fig. 6. The influence of skew angle on cogging torque.
4.3 Simulation and optimization results and comparison of cogging torque

After the optimization of the pole arc coefficient and the inclined chute angle, the higher harmonic of the induced electromotive force is reduced, which makes the waveform of the induced electromotive force have better sinusoidal. And the cogging torque suppression phenomenon is obvious, as shown in Fig. 7.

![Graph showing comparison of induced electromotive force harmonic analysis](image1)

(a) Comparison chart of induced electromotive force harmonic analysis of integer slot scheme.

![Graph showing comparison of induced electromotive force harmonic analysis](image2)

(b) Comparison chart of induced electromotive force harmonic analysis of fractional slot scheme.

**Fig. 7.** Comparison chart of no-load operation induced electromotive force harmonic analysis.

**Table 8.** Comparison of no-load induced electromotive force of the prototype.

| Design scheme       | Generator model       | RMS value of no-load voltage fundamental wave | Fundamental RMS of load phase current |
|---------------------|-----------------------|---------------------------------------------|-------------------------------------|
| Integer slot scheme | Original model        | 3284.6 V                                    | 1984.4 A                            |
|                     | Optimum pole arc coefficient | 3277.3 V                                     | 1995.8 A                            |
|                     | Optimize skew angle   | 3264.7 V                                    | 1969.1 A                            |
| Fractional slot scheme | Original model        | 938.3V                                      | 7169.4 A                            |
|                     | Optimum pole arc coefficient | 942.5V                                      | 7177.3 A                            |
|                     | Optimize skew angle   | 940.7V                                      | 7165.8 A                            |
Through the analysis of the air gap flux density waveform, induced electromotive force waveform and output current waveform of the two optimized PMSG prototypes, it can be concluded that the motor performance of the two prototypes has not decreased after the optimization of cogging torque, the permanent magnets are running in a reasonable working range, and there is no demagnetization, which can reduce the cogging torque and meet the requirements Design requirements.

5 Conclusion

This paper optimizes the cogging torque problem in the design of PMSM. Based on the combination of Taguchi algorithm and finite element analysis, the optimization method of the contrastive analysis is proposed for the two prototype under different pole arc coefficient and chute angle. The following conclusions can be obtained:

1) The orthogonal table of Taguchi algorithm is established, and it is concluded that pole arc coefficient and chute angle are the main influencing factors of generator cogging torque. The variance and influence proportion of the above two factors are used as the evaluation index of generator cogging torque amplitude.

2) According to the variation of the pole arc coefficient, the best pole arc coefficient of the generator can be obtained, and with the variation of the pole arc coefficient, the variation range of the cogging torque amplitude can be up to two times different. The results show that the cogging torque amplitude decreases with the increase of the chute angle, and the maximum difference of the cogging torque amplitude can be 6 ~ 8 times at the optimum chute angle. Therefore, the combination of the inclined slot and the best pole arc coefficient can greatly reduce the cogging torque amplitude, in order to make the operation of large capacity wind turbine more stable.
(3) By combining the finite element simulation results with Taguchi algorithm, it is verified by two prototype tests. The test results show that the design idea of megawatt wind turbines combined with skew slot and pole arc coefficient can greatly reduce the cogging torque while the performance of the generator is guaranteed, which provides a reference for the design of large-capacity wind turbines.

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