Mitigation of bias sources for atmospheric temperature and humidity in the mobile Weather & Aerosol Raman Lidar (WALI)

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Abstract

Lidars using vibrational and rotational Raman scattering to continuously monitor both the water vapor and temperature profiles in the low and middle troposphere offer enticing perspectives for applications in weather prediction and studies of aerosol/cloud/water vapor interactions by deriving simultaneously relative humidity and atmospheric optical properties. Several heavy systems exist in European laboratories but only recently have they been downsized and ruggedized for deployment in the field. In this paper, we describe in detail the technical choices made during the design and calibration of the new Raman channels for the mobile Weather and Aerosol Lidar (WALI), going over the important sources of bias and uncertainty on the water vapor & temperature profiles stemming from the different optical elements of the instrument. For the first time, the impacts of interference filters and non-common-path differences between Raman channels, and their mitigation, are particularly investigated, using horizontal shots in a homogeneous atmosphere. For temperature, the magnitude of the highlighted biases can be much larger than the targeted absolute accuracy of 1°C defined by the WMO (up to 6°C bias below 300 m range). Measurement errors are quantified using simulations and a number of radiosoundings launched close to the laboratory. After de-biasing, the remaining mean differences are below 0.1 g/kg on water vapor, 1°C on temperature, and RMS differences are consistent with the expected error from lidar noise, calibration uncertainty, and horizontal inhomogeneities of the atmosphere between the lidar and radiosondes.

1 Introduction

Atmospheric temperature and humidity in the low atmosphere are together essential to comprehend weather phenomena and their evolution in a changing climate. Through the effect of relative humidity on aerosol hygroscopicity and cloud formation, they also influence the
radiative balance of the Earth, generating the largest uncertainties in climate projections (IPCC, 2013). For both weather and climate prediction, observation means have evolved tremendously, notably with satellite retrievals of moisture and temperature routinely assimilated in numerical models. Yet remote-sensing techniques from spaceborne missions have difficulties probing the lower troposphere below 2-3 km in altitude, and have vertical resolutions that are too low, greater than 1 km in the lower troposphere (e.g. Prunet et al., 1998; Crevoisier et al., 2014). They are thus unable to resolve temperature inversions and thin dry/humid air masses (e.g. Chazette et al., 2014; Hammann et al., 2015; Totems et al., 2019). Providing complementary profiles of the important thermodynamic variables in the first kilometres of the atmosphere, where most of the water vapour and temperature vertical variability is confined, is of paramount importance for both weather forecast and reducing aerosol-induced uncertainty on climate models (Wulfmeyer et al., 2015).

Given their capacity for continuous, well-resolved and precise temperature measurements in the lower troposphere, Vibrational Raman (VR) and Rotational Raman (RR) lidars have emerged as adequate tools in this endeavour. Water vapor profilers are now well-established (from Whiteman et al., 1992 to e.g. Dinoev et al., 2013), whereas temperature profilers have recently become more widespread and powerful (from Cooney, 1972 and Vaughan et al., 1993 to e.g. Weng et al., 2018 or Martucci et al., 2021). Without tackling turbulence-scale resolution which is the prerogative of heavier systems like the Raman lidars of the University of Hohenheim (Behrendt et al., 2015), the University of Basilicata (Di Girolamo et al., 2017) or ARTHUS (Atmospheric Raman Temperature and Humidity Sounder, Lange et al., 2019), there is a need for field-deployable instruments capable of fulfilling the breakthrough requirements set by the World Meteorological Organization in terms of accuracy on atmospheric temperature and humidity in the low troposphere (WMO, 2017). Lidar profiles have proven beneficial for both numerical weather prediction (NWP) models (e.g. Adam et al., 2016; Fourrié et al., 2019), the study of dynamic processes in the planetary boundary layer (PBL) (e.g. Behrendt et al., 2015) or interactions between water vapor and aerosols (e.g. Navas-Guzmán et al., 2019). But to obtain the absolute accuracies demanded here, especially that of 1°C or less on temperature, the required accuracy on the lidar channel ratios and their calibration is extremely stringent, and the sources of systematic error seldom discussed in the literature (Behrendt and Reichardt, 2000; Simeonov et al., 1999; Whiteman et al., 2012).

Within the European lidar landscape, WALI (Weather and Aerosol Lidar) is a seasoned mobile Rayleigh-Mie-Raman system, “eyesafe” at 355 nm, first deployed during the HyMeX international field campaign and subsequently ChArMEx and PARCS, for aerosol and water
vapor profiling (resp. Hydrological cycle in the Mediterranean eXperiment, Chemistry and Aerosol in the Mediterranean Experiment, Pollution in the Arctic System; Chazette et al., 2014b, 2018; Totems et al., 2019; Totems and Chazette, 2016). In its latest evolution, the VR channels have been replaced by a Newton reflector and a polychromator also including RR channels for temperature profiling. On this occasion, we have established that biases due to various sources, in particular from the dependency of spectral filtering on the angle of incidence, detector non-uniformities and other non-common-path differences between Raman channels, may be several times greater than the requirements if left unchecked. Correctible as they are by measuring the ratios of overlap factors on the individual channels, these effects are not reported in the literature of lidar temperature measurements. However, they were bound to appear given the physical characteristics of the systems mentioned hereabove.

The aims of this paper are: i) to compile for the first time the sources of systematic error that must be considered and mitigated when using a Raman lidar to profile atmospheric temperature and humidity, ii) to validate WALI as a dependable profiler deployable for field campaigns, satisfying the requirements set by the WMO.

The theory of the Raman lidar retrieval of the atmospheric temperature and WVMR, the error budget on these parameters, and the known causes of bias are recalled in section 2, as well as the principle and limitations of the overlap measurement method. In section 3, after summarizing the characteristics of WALI, we propose a sequential review of the components of the lidar chain, characterizing and mitigating the error sources. The results of a calibration and qualification experiment using radiosondes follow in section 4. A conclusion and outlooks are presented in section 5.

2 Theoretical considerations

2.1 Raman lidar retrieval of humidity and temperature

We will introduce notations by briefly recalling the theory of the retrieval of water vapor content and temperature by the Raman lidar technique; the complete theory has been extensively derived before, by Whiteman et al. (1992) and Behrendt (2005) respectively, among others.

The vertical profiles of water vapor mixing ratio (WVMR) \( r_{\text{H}_2\text{O}} \) and temperature \( T \) are calculated from the ratios of the \( \text{H}_2\text{O} / \text{N}_2 \)-vibrational Raman (VR) channels and the RR2 (high-J number) / RR1 (low-J number) rotational Raman (RR) channels, respectively:
Signals $S_j(z)$ of Raman channels $j$ have all been previously averaged over the required altitude and time to improve the signal to noise ratio (SNR), and corrected for i) electronic baseline variations by subtracting a baseline recorded every few profiles with detector (photomultiplier tube, PMT) gain set to zero, ii) the sky background mean value assessed on pre-trigger or post-signal samples, iii) PMT gain variations (allowed on the VR channels to optimize daytime dynamic range, e.g. Chazette et al. (2014b)), iv) known leakage of the elastic return in the RR filters (Behrendt and Reichardt, 2000). $S_j(z)$ are thus expressed as:

$$S_j(z) = \frac{1}{G_j(U_j)}(S_{j,raw}(z) - \hat{L}_j(z) - \hat{B}_j) - \hat{\varepsilon}_j S_{elas}(z)$$  \hspace{1cm} (3)$$

where $G_j$ is the channel gain controlled by PMT voltage $U_j$, $S_{j,raw}$ is the raw lidar signal, $\hat{L}_j$ is the estimated baseline, $\hat{B}_j$ is the estimated sky background parasitic signal, $\hat{\varepsilon}_j$ is the estimated residual transmittance of the emitted laser wavelength through the interference filter (IF) of Raman channel $j$ compared to the elastic channel, and $S_{elas}$ is the elastic signal. $\hat{x}$ denotes the estimate of $x$.

Both $R$ and $Q$ must then also be corrected for the difference of atmospheric transmission between the two Raman channels and the ratio of overlap factors:

$$R'(z) = \frac{\exp(\Delta \tau(z))}{\bar{OR}_R(z)} R(z)$$  \hspace{1cm} (4)$$

$$Q'(z) = \frac{1}{\bar{OR}_Q(z)} Q(z)$$  \hspace{1cm} (5)$$

where $\Delta \tau(z)$ is the difference of optical thickness from the lidar until range $z$ observed between the wavelengths of the two VR channels, and where $\bar{OR}_R(z)$ and $\bar{OR}_Q(z)$ are the estimated ratios of the overlap factors of the two VR / RR channels respectively (expressed in section 2.4). With an emitted wavelength at 355 nm, $\Delta \tau(z)$ between 387 and 407 nm seldom produces deviations above 5%, and can be efficiently estimated using an average atmospheric density profile for molecular optical thickness and the N$_2$-Raman channel itself for aerosol optical thickness (e.g. Whiteman, 2003).
The WVMR is simply proportional to the VR scattering ratio between H$_2$O and N$_2$, since nitrogen gas has a constant mixing ratio in the troposphere and stratosphere. The temperature is retrieved from the more complex dependency of the RR scattering cross sections between the two channels RR1 and RR2. The respective estimates $\hat{r}_{H_2O}$ and $\hat{T}$ (to be distinguished from the true values without $^\wedge$) are obtained, after calibration, by:

$$\hat{r}_{H_2O}(z) = \hat{R}R'(z)$$

(6)

$$\hat{T}(z) = \hat{f}^{-1}(Q'(z))$$

(7)

where $\hat{R}$ is the estimate of the calibration coefficient for WVMR combining all instrumental constants. Calibration function $\hat{f}$ is the estimate of the temperature dependency of the ratio of RR cross-sections. It takes into account the instrumental constants of the two RR channels. We take the model previously selected for operational purposes by Behrendt (2005):

$$Q' = f(T) = \exp\left(a + \frac{b}{T} + \frac{c}{T^2}\right)$$

(8)

with $a$, $b$, $c$ the coefficients of a polynomial regression of ln($Q'$) as a function of $1/T$. $\hat{R}$ and $\hat{f}$ are obtained by confronting lidar profiles of $R'$ and $Q'$ with collocated in-situ measurements of $r_{H2O}$ and $T$ (e.g. from a radiosounding), aiming for a wide range of values for a better constraint on the calibration.

### 2.2 Simple error budget

In this section, we will make a first assessment of the acceptable error on $R$ and $Q$ starting from the accuracy requirements for WVMR and temperature profiles, which ensue from each scientific need, as compiled by Wulfmeyer et al. (2015) for key applications. Monitoring, verification (e.g. model qualification or calibration/validation of satellites) and data assimilation purposes can be adequately addressed by a profiler capable of i) <5% noise error and <2-5% bias for water vapor, ii) <1°C noise error and <0.2-0.5°C bias for temperature. In a simple error budget, we can use requirements of $\frac{\Delta r_{H_2O}}{r_{H_2O}}_{\text{max}} = 5\%$ for WVMR, and $\Delta T_{\text{max}} = 1^\circ$C for temperature, to give a first idea of the different expectations for the performance of a VR/RR lidar.

Eqs. (4-8) allow to derive constraints on the acceptable relative error on the corrected lidar observables $R'$ and $Q'$, for either random noise or bias, as:
The relative error on $R$ is equal to the constraint on WVMR, i.e. 5%. An assessment of the relative error on $Q$ is performed considering the RR filter parameters given in Table 2 (section 3) to yield the following numerical application: around $T_0 = 0^\circ C$, $Q'(T_0) = 0.44$ and $d Q'/dT(T_0) = +0.35/100^\circ C$, so that: $(\frac{\Delta Q'}{Q'})_{max} = 0.79\% \Delta T_{max}(^\circ C)$.

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### Table 1. Summary of accuracy requirements from Wulfmeyer et al. (2015) and corresponding constraints on ratios $R'$ and $Q'$. Resulting errors on relative humidity $RH$ at 0°C and 50%RH.

| Parameter | Random error | Systematic error (bias) |
|-----------|--------------|------------------------|
| $r_{H2O}$ | <5% relative | <2-5% relative          |
| $T$       | <1°C         | <0.2-0.5°C              |
| $R'$      | <5% i.e. SNR > 20 | <2-5%                  |
| $Q'$      | <0.8% at 0°C i.e. SNR > 125 | <0.12-0.4% at 0°C |
| $RH$      | 4.3%RH       | 1.2-2.9%RH              |
|           | at $T = 0^\circ C$, $RH = 50\%$ | at $T = 0^\circ C$, $RH = 50\%$ |

The results, summarized in Table 1, have very important implications. In order to fulfill WMO requirements for temperature and WVMR measurements, the $Q'$ ratio must be 6-10 times more accurate than $R'$. However, Raman cross-sections are larger for the RR channels than for the $H_2O$ VR channel. Hence when dealing with a RR+VR lidar rather than a VR system, the main difficulties are not only due to low signal-to-noise ratio but also encompass strong constraints linked to instrumental biases. SNR as used in Table 1 is defined on $R$ and $Q$ at the final resolution, and is calculated from the individual signal variances and means (including laser & sky-background photon noise, detection noise), as:

$$SNR_R = \left( \frac{\text{var}(S_{N_2})}{(S_{N_2})^2} + \frac{\text{var}(S_{H_2O})}{(S_{H_2O})^2} \right)^{\frac{1}{2}}$$  \hspace{1cm} (11)
\[ SNR_Q = \left( \frac{\text{var}(S_{RR1})}{\langle S_{RR1} \rangle^2} + \frac{\text{var}(S_{RR2})}{\langle S_{RR2} \rangle^2} \right)^{1/2} \]  

(12)

\[ SNR_R, \text{ typically limited by the H}_2\text{O channel, must be above } \sim 20 \text{ and } SNR_Q \text{ must be above } \sim 125 \]

to satisfy the requirements given above. Such high values can be reached by increasing the laser

power and pulse repetition frequency (PRF), or enlarging the integration over altitude and time,

as SNR is usually magnified by the square roots of the energy and number of averaged samples.

However, limits on the latter are also set by Wulfmeyer et al. (2015) for the same applications;

integration range \( \Delta z \) should be below 100 m in the PBL and 300 m in the lower free troposphere,

whereas an integration time \( \Delta t \) between 15 (assimilation and verification) and 60 min

(monitoring) is required.

We derive the errors expected on RH given those on temperature and WVMR at the bottom of

Table 1. Here and in the following, \%RH denote absolute percentage units on RH, whereas %

denote relative errors. Relative humidity is derived as a function of atmospheric pressure,

temperature and WVMR, using standard empirical relationships for the water vapor saturation

pressure. Here, we use the Buck equation (Buck, 1981), which is accurate within 0.2% between

\(-40^\circ \text{C and } +100^\circ \text{C}:

\[ P_{wv,\text{sat}} = 6.1121 \frac{T}{T + 257.14^\circ \text{C}} \exp \left( 18.678 \frac{T}{T + 234.5^\circ \text{C}} \right) \]  

(13)

\[ RH = \frac{P}{P_{wv,\text{sat}} r_{H_2O}} r_{H_2O} + 621.991 \text{ g kg}^{-1} \]  

(14)

with \( P \) pressure and \( P_{wv,\text{sat}} \) the water vapor saturation pressure in hPa, \( T \) temperature in \(^\circ \text{C}.

\[ 2.3 \text{ Sources of bias} \]

Biases arising from inaccurate measurement of any of the estimated factors of Eqs. (3-7), or

from a variation after that measurement due to instabilities in the instrument, must also be

smaller than the aforementioned values of 2-5\% for WVMR and 0.12-0.4\% for temperature,

the latter being especially difficult to reach. Their impact must be mitigated either by careful

design or by precise estimation.

The expected (i.e. noiseless) values of \( R \) and \( Q \) can be detailed as:

\[ \overline{R(z)} = \frac{O_{H_2O}(z)}{O_{N_2}(z)} \frac{K_{H_2O}}{K_{N_2}} \frac{\sigma_{H_2O}}{\sigma_{N_2}} r_{H_2O}(z) \]  

(15)
\[
\bar{Q}(z) = \frac{O_{RR2}(z) K_2 \sigma_{RR2}(T(z))}{O_{RR1}(z) K_1 \sigma_{RR1}(T(z))}
\]  
(16)

with \(\bar{x}\) denoting the expected value of variable \(x\), \(K_j\), \(\sigma_j\) and \(O_j(z)\), the instrumental constant, Raman backscatter cross-section, and overlap factor of channel \(j\), respectively. To simplify our discussion, we choose to incorporate any deviation that affects the ratios without a range-dependence into the instrumental constant ratio, and any deviation with a range-dependence into the overlap ratio.

As previously explained, the impact of deviations on variables in Eq. (15) remains tolerable below a few percent, but for the distinctly more constrained temperature retrieval, the variables in Eq. (16) are affected by the following effects that directly induce significant bias:

- Laser wavelength drift or filter central wavelength (CWL) drift with temperature both affect the ratios indiscriminately with range. By simulating the variation of \(Q\) with the WALI filter parameters (section 3), we find a large impact of a wavelength drift \(\Delta \lambda\) (measured between the laser on one side and both interference filters on the other side):

\[
\frac{d\bar{Q}}{\bar{Q}} / d\lambda \approx -0.26 \text{ pm}^{-1} \text{ and } \Delta T \approx -0.34 \text{°C pm}^{-1} \Delta \lambda,
\]

meaning just 3 pm drift in either filter or laser wavelengths can lead to biases above 1°C. That is one of the reasons why the laser must be frequency-stabilized. Also, IFs subjected to fluctuations of local temperature are known to experience CWL drifts; for WALI’s filters manufactured by Materion, this amounts to 1.28 pm °C\(^{-1}\) (value given by the manufacturer after their material dilation simulation). The temperature of the polychromator must thus be kept stable within 1°C for this bias to become negligible.

- Filter CWL variation with angle of incidence (AOI) on the IF generates a channel transmittance variation which is range-dependent, and different for each filter. Indeed, this variation \(\Delta \text{CWL}\) is approached by (e.g. Hayden Smith and Smith, 1990):

\[
\Delta \text{CWL}(\theta') \approx \text{CWL} \frac{\theta'^2}{2n_{\text{eff}}^2}
\]

(17)

where \(\text{CWL}\) is the filter central wavelength, \(\theta'\) is the angle of incidence on the filter (assumed small), and \(n_{\text{eff}}\) is the effective refractive index of the filter. For the RR1 filter \((n_{\text{eff}} = 1.62)\), we obtain as much as \(\Delta \text{CWL}(\theta') \approx 43 \text{ pm} \theta' (°)^2\). The problem stems from the fact that because the filter is in the pupil plane, after collimation of the received beam, each angle of incidence corresponds to a different point in the focal plane of the
receiver, which in turns corresponds to a field angle $\theta$ of the lidar, as seen on Figure 1

\[ \theta' = \frac{f}{f'} \theta > \frac{D_{\text{rec}}}{D_{\text{IF}}} \theta \]  

(18)

where $f$ and $f'$ are the receiver/recollimation focal lengths, $D_{\text{rec}}$ and $D_{\text{IF}}$ are the receiver and IF diameters. For a 150-mm diameter receiver using a 1-inch diameter (22 mm clear aperture) IF, we obtain at least $\theta' = 0.39^\circ$ for a $\theta = 1$ mrad field angle, producing $\Delta \text{CWL}(\theta') \approx 6.6 \text{ pm}$ and already $\Delta T \approx 2.2^\circ \text{C}$. Note that the impact gets proportionately larger with the diameter of the receiver. Because the optical path of each channel is independently aligned, this always induces different overlap factors even when sharing the same telescope. This large effect must be calibrated and corrected, yet its impact was never discussed before in the RR lidar literature, despite being three times as large in other systems with 450 mm receivers. This impact can be mitigated by attacking the filters at normal incidence, where the derivative of CWL as a function of AOI (see Eq. (17)) is minimal.

Figure 1. a) Definition of useful parameters for field angle $\theta$ and filter angle of incidence $\theta'$ calculations. $f$: receiver focal length, $D_{\text{rec}}$: receiver diameter, $\phi$: full lidar field-of-view, $f'$: collimation focal length, $D_{\text{IF}}$: IF diameter. b) Definition of metrics for overlap calculations. $e$: emitter-receiver separation, $H$: hyperfocal distance, $z_e$: entry distance of laser into field-of-view. Green/red/blue lines represent rays from infinity/finite distance/offset emitted beam, respectively.
Detector response non-uniformity up to ±12%, both as a function of impact point on the active surface and of angle of incidence, is now specified on the cathodes of PMTs used at 400 nm wavelength (Hamamatsu (2007), Section 4.3.3). The amplitude was found to be much larger by Simeonov et al. (1999), with significant impact. This effect has been bluntly limited in all our lidars by putting the cathode plane as far as possible before the focal plane, while still avoiding vignetting. It can still be responsible for differences of overlap factors between channels.

Uncalibrated PMT gain or digitizer baseline variations will of course induce bias in the channel system constants. We will see how to mitigate these effects.

Slight variations of overlap or channel transmittance after calibration will be directly responsible for bias. In the next sub-section, we discuss how they can appear.

2.4 Overlap measurement with horizontal shots and limitations

Range-dependent biases influence the lower part of the lidar profiles exactly like the overlap factors. They significantly impact the profiles up to a given range from the emitter, depending on the characteristics of the receiving optics as seen above, but also on the quality of the alignments, which is seldom twice the same. Two methods are used in the literature to approximate the actual overlap factors of a Raman lidar: i) an iterative Klett inversion of elastic and Raman channels sharing the same telescope is easy to achieve (Wandinger and Ansmann, 2002) but inefficient when non-common path errors are involved, whereas ii) the method of aiming the lidar horizontally (e.g. Sicard et al., 2002; Chazette and Totems, 2017) is sometimes impractical but more direct and yields more accurate results in an horizontally homogeneous atmosphere over a range of 1 to 2 km. In the context of RR measurements, it is necessary to implement the latter, and also to measure the ratios of overlap factors, rather than the overlap factors themselves, thus avoiding errors due to an imprecise estimation of atmospheric extinction.

Considering a horizontal line of sight in a supposedly homogeneous atmosphere, the expected values of ratios $R$ and $Q$ can be expressed as:

$$
\overline{R}(z) = R(z_\infty) \frac{O_{H_2O}(z)}{O_{N_2}(z)} \exp(-\Delta \alpha \cdot z)
$$

(19)

$$
\overline{Q}(z) = Q(z_\infty) \frac{O_{RR2}(z)}{O_{RR1}(z)}
$$

(20)
where $R(z_{\infty})$ and $Q(z_{\infty})$ are the values observed when all overlap factors have become constant at a sufficiently large range from the lidar, noted $z_{\infty}$, after which variations of the optical path inside the reception channels become negligible. $\Delta \alpha = \alpha(407\text{nm}) - \alpha(387\text{nm})$ is the difference of atmospheric extinction between the two VR wavelengths.

To evaluate $z_{\infty}$, we introduce in Figure 1 b) parameters that characterize the overlap of a paraxial or coaxial lidar (e.g. Kuze et al., 1998): i) $z_{e} = 2e/\phi$ at which the emitted laser beam located at distance $e$ from the receiver axis enters the field of view, whose full size is $\phi$; $z_{e}$ is null for a coaxial system ii) $H = D_{rec}/\phi$, the so-called hyperfocal distance, minimum range from which the beam originating from a point still fully enters the field stop; iii) $H_{IF} = 2D_{rec}/f\theta_{max}'$, that we might call the filter hyperfocal distance, similarly to the former, the minimum range from which the image of a point does not exceed $\theta_{max}'$, the AOI on the IF that significantly changes its transmittance. $z_{\infty}$ is above the maximum of those three, which is usually $H_{IF}$. If we use for $\theta_{max}'$, the AOI value causing 1°C bias on temperature per Eq. (10) and Eq. (15), we find: $z_{\infty} > H_{IF} = 780 \text{ m}$. Note that $z_{\infty}$ can reach several km with misaligned filters.

If for instance the lidar can be mounted on a rotating platform capable of aiming horizontally, the overlap ratios $OR_{R}(z) = O_{H20}(z)/O_{N2}(z)$ and $OR_{Q}(z) = O_{RR2}(z)/O_{RR1}(z)$ can be estimated with suitable precision ($\sim 10^{-3}$) by averaging the signals over time and smoothing them over range, and finally correcting for differential of extinction on the VR ratio:

$$OR_{R}(z) = \frac{R(z)}{R(z_{\infty})}\exp(\Delta\alpha \cdot z)$$  \hspace{1cm} (21)

$$OR_{Q}(z) = \frac{Q(z)}{Q(z_{\infty})}$$  \hspace{1cm} (22)

These estimates of the overlap ratios will then be used during signal processing for vertical shots as in Eq. (4) and (5). However, assumptions are made for the former estimation, namely:

- As explained above, the atmosphere is assumed to be homogeneous in WVMR and temperature (down to $<0.5^\circ\text{C}$) up until $z_{\infty}$, whereas the overlap ratios must be constant (down to $<0.4\%$) after $z_{\infty}$. Also, the maximum range (with sufficient SNR) of the lidar must exceed $z_{\infty}$, implying nighttime measurements for the Raman channels. Therefore, the effects generating overlap variation after a few hundred meters must be prevented.

- The lidar is assumed to retain the exact same overlap functions when aiming horizontally and vertically. Considering a field of view around 1 mrad, the stability of the emission and reception optical paths must be better than $\sim 10 \mu\text{rad}$ between these
two positions. This is feasible for a small refractor but difficult for a Raman system such as WALI, with a heavy laser and large reflector.

These difficulties make it extremely challenging to estimate the overlap ratios with an accuracy better than a few percent. This is enough for the WVMR, but we find that a correction must be applied by comparing with in-situ sounding for temperature measurements by Raman lidar.

3 Implementation and bias mitigation on the WALI system

In this section, we describe the WALI instrument from the emitter to the reception channels, characterizing the critical elements in the framework of WVMR and temperature measurements. The system has evolved from its previous implementation described in Totems et al. (2019), by adding RR channels and a fibered telescope receiver. A global diagram presenting the main lidar sub-systems is shown in Figure 2, and a summary of its characteristics is given in Table 2.

Figure 2. Global diagram of the lidar system. The main sub-systems are: the emitter (center), the elastic receiver using a refractor (top), the Raman receiver using a fibered parabolic reflector (bottom), and a separate, thermally stabilized polychromator (upper right). See Figure 5 for the detail of the polychromator design.

Its main features are a single rotatable platform (lightweight carbon fiber breadboard by CarbonVision GmbH) carrying both its emission and reception paths, a 150-mm refractor for the elastic channels (for aerosol studies), and a 150-mm diameter parabolic fibered reflector for all the Raman channels. The separation of the four Raman channels takes place in a deported polychromator set in a thermally controlled enclosure, fed by the optical fiber. Fiber optics are
also known to partly scramble the input illumination, which could help minimize the range-
dependance of filter transmittance or detector sensitivity for the different Raman channels. The
output signals from the photomultiplier tubes (PMTs) in the polychromator are digitized by a
NI™ PXI system (not shown).

Table 2. WALI instrument characteristics summary (PRF: pulse repetition frequency, FOV:
field of view, CWL: central wavelength in vacuum, FWHM: full width at half-maximum, OOB:
out-of-band blocking specification, OD: optical density)

| Emitter | Laser |
|---------|-------|
|         | Lumibird™ Q-Smart 450 SLM, tripled Nd:YAG, frequency stabilized $\lambda_{\text{laser}} = 354.725$ nm in vacuum, $E_p = 100$ mJ, PRF = 20 Hz. |

| Optics | High-power polarizing beamsplitter and 10x beam expander |
|--------|----------------------------------------------------------|
|        | Output beam diameter: 65 mm, Em/Rec separation: 200 mm |

| Elastic | Optics |
|---------|--------|
| receiver | Ø150 mm F/2 UV fused-silica refractor |
| Spatial filter | 0.67 x 2 mrad FOV |

| Spectral filter |
|-----------------|
| CWL = 354.71 nm, FWHM = 0.22 nm, OOB: OD >4.0 |

| Raman | Optics |
|-------|--------|
| receiver | Ø150 mm F/4 Newton reflector |
| Spatial filter | Ø1.67 mrad FOV |

| Fiber optics |
|-------------|
| Ø1 mm, 2-m long, OH-rich multimode fiber |

| VR spectral filters |
|---------------------|
| 365 nm longpass (OD >2) + 395 nm (OD >2) beamsplitter + Materion™ interference filters: |
| N₂: CWL = 386.76 nm, FWHM = 0.27 nm, OOB: OD >4.0 |
| H₂O: CWL = 407.59 nm, FWHM = 0.34 nm, OOB: OD >4.0 |

| RR spectral filters |
|---------------------|
| 365 nm shortpass (OD>2) + |
| CWL = 355 nm, FWHM = 10 nm, flat-top, OOB: OD >6.0 + 50:50 non-polarizing beamsplitter + Materion™ interference filters: |
| RR1: CWL = 354.09 nm, FWHM = 0.24 nm, OD >6.0 at 354.7 nm |
| RR2: CWL = 353.22 nm, FWHM = 0.54 nm |

| Detection | Photodetectors |
|-----------|---------------|
|           | Hamamatsu H10721-210 photomultiplier tubes (PMT) with >0.13 A/W cathode sensitivity |

| Amplification |
|---------------|
| Up to 2 10^6. Elastic & RR: fixed, VR: sky-background piloted |

| Acquisition |
|-------------|
| 3x NI™ PXI-5124 two-channel digitizers |

| Sampling frequency: 200 MHz, 12-bit, Q-switch-triggered |
3.1 Emitter

The emitter is a commercial Lumibird/Quantel “Q-Smart 450” Nd:YAG pulsed laser, stabilized by injecting the output of a single longitudinal mode fiber laser emitting at 1064.175 nm into the main cavity (“SLM” option), and frequency-tripled to emit at wavelength $\lambda_{\text{las}} = 354.725$ nm (in vacuum). The nominal pulse energy for the Q-Smart 450 with SLM is 100 mJ at 355 nm, with a Pulse Repetition Frequency (PRF) of 20 Hz. These values set WALI near the eye safety limit for pulsed energy, making the system eyesafe at the output of a 2-meter funnel, as limited by leaks at 532 nm through the built-in filtering dichroic plates.

A critical issue to be cleared before using the Q-Smart 450 SLM in WALI was the spectral purity and stability of the laser, in terms of linewidth and wavelength drift. The laser seeder at 1064.175 nm is specified with a 50 MHz ($0.062$ pm at 355nm) stability at fixed temperature, and $37$ MHz °C$^{-1}$ ($0.046$ pm °C$^{-1}$ at 355 nm) temperature drift. Nevertheless, the stability of the Q-Smart emission at 354.725 nm has been verified with a dedicated optical setup, sending the output of a Michelson interferometer with optical path differences (OPD) between 0 and 100 mm on a UV-sensitive CCD camera. By extracting the contrast and phase variations of the fringes at large OPDs from the videos, we were able to ascertain:

- the laser linewidth, without seeder, to be 24±2 pm (versus 26.5 pm datasheet value), and with seeder, to be small compared to 1 pm (versus 0.2 pm datasheet value),
- the wavelength drift, without seeder, to be below 8 pm over 10 minutes, and with seeder, to be below 0.2 pm RMS (root mean square fluctuations) over 5 minutes. We consider the remaining fluctuations to be mostly due to the ~0.05 pm °C$^{-1}$ temperature-linked drift of the seeder, which is not temperature-controlled and was recently turned on.

Given the requirements derived in Section 2.3, this makes the seeded Q-Smart laser theoretically suitable for RR measurements of temperature.

3.2 Raman receiver

In this sub-section we discuss the possible impact on the VR/RR ratios of the fibered reflector (beam scrambling and fiber optics fluorescence), of Raman filters characteristics, and of the
polychromator design and alignment. As far as we know, this type of comprehensive study does not exist in the literature for Raman lidars.

3.2.1 Fibered reflector telescope and scrambling of the lidar field-of-view

The elastic and Raman receivers are both 150 mm in diameter. The focal length of the refractor (elastic channels) is ~300 mm, which with a 200x600 µm field stop achieves full overlap at ~150-200m. However, the focal length of the reflector (Raman channels) is 600 mm (parabolic mirror with aperture F/4); this implies using a multimode fiber optics about 1 mm in diameter as the field stop to allow similar results in terms of field-of-view and overlap. The chosen fiber optics is an OH-rich UV fused silica fiber, 2 m in length and 1000 µm in core diameter, with numerical aperture 0.22 (Avantes FC-UV1000-2).

Coupling the reflector output into a multimode fiber (e.g. Chourdakis et al., 2002) allows: i) to minimize occultation of the primary mirror (here only 12 mm in diameter), ii) to deport the Raman channel separation away from the telescope, making it a separately tunable optical system, minimizing the overall lidar size and making light or temperature confinement easier, iii) in theory, to scramble the fiber output illumination versus the lidar field angle, therefore minimizing the range-dependence of AOIs on the IFs discussed in Section 2.3, and flattening overlap ratios after the geometrical full-overlap distance.

The scrambling of the lidar field-of-view, via the multiple internal reflections in the fiber, has been experimentally tested by imaging the output of the fiber, with a varying point-like input. The results are shown in Figure 3. Note that the radial coordinate of the output point relative to the center of the fiber corresponds to a given AOI on a well-aligned IF in the following polychromator, after a $f' = 50$ mm doublet lens.
Figure 3. Images of the output facet of the 1 mm diameter multimode fiber optics for a) centered and b) decentered (at $x_m = 0.38$ mm horizontal offset from the center of the core) input point of a 20-mm beam focused on the input facet of the fiber, and energy density profiles along the x and y axes.

It appears on Figure 3 b) that the input energy is mostly redistributed tangentially (i.e. along the angular polar coordinate, as opposed to radially) by its passage through the fiber. The radial dispersion remains small, and the mean output radius is approximately equal to the input radial coordinate. Manually applying curvature to the fiber, as suggested by so-called “mode scrambling” devices, did not make the energy distribution more uniform so much as creating unwanted losses (effect not shown). Even for a centered input, the energy radial distribution – i.e. the percentage of the total output in a given radial bin, that will therefore impact a well-aligned filter at the same AOI – is uniform. We conclude that even with the use of fiber optics the angle of incidence on the interference filters depends on the image positions in the focal plane of the telescope (i.e. mainly the distance to the optical axis), in contrast to what could be expected. Range-dependent biases will not be strongly mitigated.

3.2.2 Fiber optics fluorescence

It has been shown by Sherlock et al. (1999) and discussed by Whiteman et al. (2012) that fiber optics fluorescence could be an obstacle to water vapor measurements, because elastic scattering at 532 nm was inducing fluorescence in an OH-poor fiber at a non-negligible level compared to the atmospheric Raman scattering. It was solved by using an OH-rich fiber, but it was predicted in the latter work that the effect could be larger at 355 nm.

We have characterized this effect in the WALI fiber optics, using a narrowband CW laser excitation centered at 355 nm. The output of the fiber was analyzed by a Fourier transform spectrometer (Thorlabs OSA201C spectrum analyzer), behind a longpass dichroic plate cutting the direct laser emission, and the same collimating achromat as in the polychromator. The resulting spectrum is shown in Figure 4.

We plot both the raw spectrum and the Fourier transform spectrometer noise floor after 1000 profile integrations, to highlight the very weak features observed at 780 to 910 nm, and the high associated uncertainty. Due to the noise level, and given the dichroic plate residual transmittance of the laser wavelength, we can only ascertain that the fluorescence power spectral density (PSD) around 400 nm is lower than $10^{-6}$ times the peak laser PSD, although no feature can be detected in this spectral domain. Note that fluorescence between 400 and 500 nm was indeed observed using a broadband excitation from a fibered LED at 340 nm (not shown).
Nevertheless, the amount of rejection observed for a 355 nm excitation is sufficient to exclude an adverse impact of the OH-rich fiber optics for Raman lidar measurements.

Figure 4. 1000-µm diameter, 2-meter long fiber fluorescence measurement with 355 nm laser illumination.

### 3.3 Raman channels

#### 3.3.1 Polychromator configuration

The RR+VR polychromator configuration used in WALI is presented in Figure 5. Dichroic and non-polarizing beamsplitters are used to separate the channels. In contrast to the design of Hammann et al. (2015) which optimizes throughput and laser-line rejection on the RR channels, we chose to implement a splitter-based configuration, favouring a compact system (25x25 cm, easier to confine) and normal incidence on the filter, at the expense of SNR. Indeed, designing the filters for a correct CWL at 5° incidence (as in the cited work) instead of 0° dramatically narrows the filter angular acceptance, as can be deduced by deriving Eq. (15) as a function of incidence $\theta'$. In the WALI polychromator, the output from the fiber is collimated by a near-UV achromat with 50 mm focal length, resulting in a 22 mm diameter beam. Dichroic beamsplitters with adequate cut-on wavelengths are used to separate channels. On each separated channel, an aspheric lens condenses light on the PMT surface, located 4 mm before the focal plane. A steel
cage system assembly holds all parts with great stability, however beamsplitters are not always perfectly aligned at 45° in the stock cage cubes. That is why all filter, lens and PMT sub-assemblies are mounted on tiltable mounts to allow precise alignment at normal incidence.

Figure 5. Compact rotational & vibrational Raman separation configuration used in WALI. IF: interference filter (with CWL - FWHM given in nm), BS: beam splitter, LPD: long-pass dichroic beamsplitter (with cut-off wavelength given in nm), PMT: photo-multiplier tube. This polychromator is thermally regulated in a dedicated light-tight enclosure.

3.3.2 Filters qualification

All interference filters were custom-made by Materion, including the RR filters on specifications graciously shared by the team of A. Behrendt (following Hamann et al., 2015). They were characterized on the Fourier transform spectrometer (described in section 3.2.2) prior to mounting, using fibered LEDs peaking at 340, 385 and 405 nm as the light source; the beam was collimated by the same near-UV achromat with 50 mm focal length. We give the measurements results for the RR filters in Figure 6 and Table 3.

The effective index and angular acceptance of the filters (arbitrarily chosen for a 10% loss at the CWL) were assessed by tilting the filters of a known angle. A critical parameter, the transmittance of both filters at the laser line $\lambda_{\text{laser}}$ in operational conditions was assessed on the lidar itself, by measuring the energy of an echo on a hard target located at 200 m, and switching between an elastic IF of known transmittance with a known strong optical density and the RR IF in question. The excellent extinction in the RR1 filter guarantees a minimal effect of elastic signal leak in temperature retrievals, but it was nevertheless subtracted as in Eq. (3). Note that no significant echo was detected on the H$_2$O-Raman channel, indicating extinction better than a few $10^{-9}$, thanks to the two dichroic plates.
Figure 6. RR filters spectral transmittance measured on optical spectrum analyzer with illumination by a 340 nm LED: RR1 (low-J) and RR2 (high-J) filter at 0° incidence.

Table 3. Measured RR IF characteristics. All CWL values are given in vacuum.

|                  | RR1 filter | RR2 filter | Uncertainty |
|------------------|------------|------------|-------------|
| CWL              | 354.09 nm  | 353.22 nm  | 0.01 nm     |
| FWHM             | 0.24 nm    | 0.54 nm    | 0.01 nm     |
| \( n_{eff} \)    | 1.62       | 2.03       | 0.05        |
| Max transmittance| 69%        | 51%        | 5%          |
| Laser line transmittance | \( 2.7 \times 10^{-8} \) | \( 2.9 \times 10^{-7} \) | 10% relative |
| Angular acceptance | 1.5°       | 2.5°       | 0.2°        |
| (AOI for 10% loss at CWL) |           |            |             |
| CWL shift at max field angle | -9.8 pm | -2.5 pm | 0.3 pm |
| (i.e. edge of fiber, AOI = 0.59°) |           |            |             |

3.3.3 Polychromator alignment and qualification

Due to the filter CWL shift evolving as the square of the AOI in Eq. (15), it is essential to minimize range-dependent biases by aligning the filters at a precisely normal incidence from the input beam. However off-the-shelf beam splitter plate holders are found to be misaligned.
by up to 1° from an ideal 45° incidence. All PMTs are mounted jointly with their own IF and lens into a tiltable mount to correct for this (represented on Figure 7).

The alignment of these mounts is performed in the lab by conjugating an input multimode fiber of 600 µm diameter replacing the lidar input, into a target fiber 200 µm in diameter at the focus of the PMT lens, through the polychromator. Fibered LEDs are used for illumination like in section 3.3.2. All the channels are sequentially addressed in this manner. By obtaining a maximal energy and a radially uniform profile at the output of the target fiber, one can ensure alignment with a precision of 0.1 to 0.3°.

Figure 7. Method for polychromator alignment validation. Light from LEDs is input in the WALI fiber optics, passes through the polychromator, and into a multi-mode fiber (MM fiber, Ø600 µm) analysed by a Thorlabs OSA201C Fourier transform spectrometer. Channel central wavelengths are expected not deviate from those of the filter measured independently at normal incidence, to validate alignment.

To verify the result, the spectral transmittance of the polychromator channels themselves are characterized by the Fourier transform spectrometer, as shown on Figure 7. By illuminating the channel with a LED coupled in the actual lidar fiber, we ensure that the polychromator is studied in operational conditions. The CWL of each channel is expected not deviate by more than 20 pm (twice the empirical accuracy) from the CWL measured on the individual filter at normal incidence, to validate the alignment. The polychromator aligned using the procedure proposed above passes this test.

### 3.4 Detectors

Hamamatsu 10721P-210 PMTs, with >0.13 A W⁻¹ cathode sensitivity at 400 nm, and up to ~2 10⁶ controllable internal gain, are used to transform the optical flux into an electric current, directly digitized at 200 MHz (0.75 m sampling along the line of sight) by three NI PXI-5124
two-channel digitizers with 50 Ω load. The acquisition software, custom-made with Labview, conducts analog and photon-counting (thresholding at ~3 standard deviations of the noise) accumulations in parallel during 1000 shots (50 seconds), every minute, which are then pre-processed and recorded (~10 seconds down time). Every ~8 minutes, baselines are recorded with PMT gains set at zero. The next sub-sections describe critical points of the detectors affecting the RR and VR channel ratios.

3.4.1 PMT response variability

As explained in Section 2.3, the non-uniformity of the PMT response can affect the ratios of Raman channels as a function of range. We tested the sensitivity profiles of WALI’s H₂O-Raman PMT to continuous laser illumination at 405 nm wavelength, first using a 1-mm diameter collimated beam, as a function of both point and angle of incidence. A cumulated ~6.0 neutral density filter was used to avoid saturation of the PMT.

As shown on Figure 8 a), a strong variation of sensitivity by a factor of almost 2 is found on the PMT surface, much larger than specified. The relative sensitivity is lowest near the center of the PMT and highest on the sides, on a diameter of 4 mm approximately equal to the spot size in the lidar. Indeed the PMT surface is 4 mm before the focal plane of the 0.5 NA condensing aspheric lens. This is consistent with the results of Simeonov et al. (1999) on an older generation of detectors, excluding a suspected hole-burning phenomenon over the lifetime of our PMT. On the vertical axis, we also note the effect of the gridded cathode. Note that sensitivity does not vary by more than a few percent as a function of angle of incidence (not shown).

Figure 8. Study of the non-uniformity of the PMT response: a) as a function of point of impact on the active area along the horizontal (blue) and vertical (red), with a 1 mm collimated beam from a 405 nm laser, b) as a function of angle of incidence on the lens and PMT assembly similar to the ones used in the WALI polychromator, with a 22 mm collimated beam from the
same laser. Dashed lines represent uncertainty calculated over multiple measurements. Sensitivity is given normalized by its value at the approximate mechanical centre of the PMT or at normal incidence as determined using the reflection on the attached neutral density filter.

We then put the condensing lens used in the polychromator in front of the PMT, and studied its response as a function of AOI on the lens+PMT assembly, which is shown in Figure 8 b). The input beam was the nominal size in the polychromator ie. ~22 mm in diameter. We find that the curve corresponds well to the measured sensitivity profile, smoothed by its convolution with the spot on the PMT. The problem is that at normal incidence, the derivative of sensitivity with incidence is 2-5% per degree. Using the calculations in Section 2, a \(\theta = 1\) mrad field angle corresponds to 0.39° incidence on the PMT, inducing potentially 0.8-2% bias on \(R\) and \(Q\), and thus a significant 1 to 2°C bias on temperature. In the future, the condensing lenses will be replaced with afocal beam reducers to reduce this dependency.

3.4.2 Baseline and EM parasites correction

The baseline induced by the detection chain is found to vary between channels and in time. It is also subject to electro-magnetic (EM) interference causing parasitic signals of both high frequency, mostly due to the flashlamp high peak current radiating over the system, and low frequency, probably due to other neighboring electronics. For this reason, the channel baselines are evaluated regularly (by averaging 1000 shots with PMT gain set to zero, every 8 minutes), smoothed and corrected (\(L_j\) in Eq. (2)). However, for the Raman channels (H₂O and RR2 specifically), the weakness of the signals requires a specific care of EM compatibility, as repeating parasitic spikes were found to jam the channels (especially photon counting which relies on thresholding) starting at altitude 6-7 km.

Figure 9 a) shows an example of perturbed baseline. Trial and error established that common methods to avoid ground loops were not all efficient: star grounding of the various cables worsened the problem, whereas physically separating coaxial signal cables from direct current power supply and control voltage cables, and grounding all connectors and opto-mechanics again on the breadboard side, mitigated it, reaching the baseline plotted in Figure 9 b). Note that baseline variation is not significant between successive evaluations without an external perturbation; the estimated baseline is automatically subtracted from the profiles before recording during the next 8 minutes (Eq. (3)).
Figure 9. Analog detection baseline measurements (red) over 1000 laser shots with PMT gains set to zero, expressed in photon counts equivalent on the RR2 channel: a) in an unfavorable case (no mitigation), showing both baseline fluctuations over time (20 km ~ 133 µs) and strong electro-magnetic parasites at large distance; b) on the WALI system, after mitigation. The final estimated baseline ($\tilde{L}_j(z)$ in Eq. (3)) obtained after smoothing, which is subtracted to all recorded profiles, is in black.

3.4.3 PMT gain adaptation

On each channel, PMT internal amplification gain $G$ (using photoelectron multiplication) is a definite function of its control voltage $U$. The variation of $G$ by ~2 orders of magnitude allows for the optimization of the dynamic range. This helps deal with the different Raman cross-sections in each filter, with variations of atmospheric transmittance, and especially with sky background levels during daytime. The gain is pushed at its maximum possible value still satisfying two conditions: i) the signal voltage maximum does not exceed the range of the digitizer, ii) the sky background signal does not exceed the maximum output current of the PMT that guarantees linearity (100 µA, ie. $<S_{raw}> < 5$ mV). This is indispensable for day-round measurements of WVMR, otherwise the channels would be saturated during daytime (Chazette et al., 2014b), or suboptimal in SNR during nighttime.

However, PMT gain adaptation leads to biases on the Raman channel ratios if the gain versus control voltage characteristics are not known with a better precision than the requirements stated in Table 1 (2% on VR channels, 0.4% on RR channels). In Figure 10 a), we show the experimental calibration of $G$ versus $U$ as well as second-degree polynomial fits for each channel. The relative error on the VR and RR channel gain ratios approximated by these models is plotted on Figure 10 b), with the measurement uncertainty. This uncertainty is mostly due to
variations of atmospheric parameters and laser energy during calibration. Since all relative
errors are well centered, we compute that the possible error for the gain ratio with these models
is ~1.3 %. This is compatible with WVMR measurements but not with temperature
measurements. Therefore, the PMT gain should only be adapted on the VR channels, and the
RR channels should be kept at a fixed value of gain.

Figure 10. Calibration of PMT gain $G$ versus control voltage $U$: a) log-gain measurements and
second-degree polynomial model for all Raman channels, and b) relative gain ratio error
between model and measurements for vibrational and rotational Raman channel ratios.

### 3.4.4 Merging analog and photon-counting signals

Both analog and photon-counting raw signals are recorded. The analog signal has lesser SNR
at high altitude during nighttime, whereas the photon-counting signal is saturated at low altitude
and by daylight; by merging them correctly, an optimal SNR can be obtained (Newsom et al.,
2009). For signal processing, the photon-counting raw signals are first desaturated (details in
Chazette et al., 2014b). Merging is performed during nighttime on the pre-processed signals
defined in Eq. (3). After calculating a photon to Volts conversion constant at an altitude where
photon-counting is not saturated, the converted photon-counting profile replaces the analog
profile after a predefined altitude depending on signal strength (from 1 km for the $\text{H}_2\text{O}$ VR
channel, up to 4 km for the elastic channel).

We wish to emphasize here that baselines $L_j$ and background signals $B_j$ in Eq. (3) must be
estimated separately for the analog and photon-counting recorded profiles (which have no
baseline, and a smaller but non-zero background value due to the suppression of electronic noise. Otherwise, the merged signal will show discontinuities at the cut-off altitude, and biases at high altitude at dusk and dawn. Their impacts are typically much larger than the requirements of Section 2.2.

4 Qualification on the atmosphere

In this section, we qualify the WALI system starting with the measurement of its overlap factor ratios, followed by its calibration and comparisons with radiosoundings. Remaining biases are highlighted and corrected, and experimental measurement errors are evaluated.

4.1 Experimental set-up and strategy

We put the lidar into operation in our laboratory near Saclay (48°42'42"N 2°08'54"E) over a period of two weeks in May 2020. It was placed on a rotating platform below a trapdoor equipped with silica windows for zenith shots, and in front of a window at a height of about 9 m above the ground level (agl) for horizontal shots. During the latter, the lidar aimed North <5° above the horizon (beam elevation <80 m per km of range). In that direction, land use is fields up to 800 m range, buildings and trees between 800 and 2 km range, and fields again up to 5.5 km range.

To calibrate and qualify the lidar measurements, we use radiosoundings launched two to three times daily from the operational Météo-France station located in Trappes (48°46'27"N 2°00'35"E), 12.3 km WNW from the lidar near Saclay, approximately upstream in the prevailing winds, although the wind was oriented mostly NE during the May 2020 period.

4.2 Measurement of overlap ratios with horizontal shots

The overlap factors and their ratios were estimated on signals averaged over 3 hours after sunset on December 19th, 2019, with a tepid (14°C), non-turbulent but hazy atmosphere (aerosol extinction coefficient 0.32 km⁻¹ at 355 nm with Angström exponent ~1.5, 11°C ground temperature, and WVMR at ground level around 6.5 g kg⁻¹). With a planetary boundary layer (PBL) height of ~900 to 1000 m, and slow gradients of temperature (−1 to −4°C km⁻¹) and WVMR (−0.8 to −1.2 g kg⁻¹ km⁻¹) in that PBL (as measured by radiosoundings launched from Trappes at ~12:00UTC and 0:00UTC, presented in the next subsection), conditions were excellent for a homogeneous atmosphere within the first 5 km at least.
The estimated overlap factors of the different channels, with atmospheric extinction fitted between 800 and 2000 m, are shown in Figure 11 a). Full geometrical overlap is obtained as expected between 150 and 200 m, but the curves differ by several percent between the Raman channels. Atmospheric extinction drifts from the estimated value after 2 km.
Figure 1. a) Overlap factors measured over 3 hours of nighttime measurements with a horizontal line-of-sight on Dec. 19, 2019. Estimated overlap ratios between VR (b) and RR (c) channels: native resolution (thin blue line), final estimate after smoothing (thick red line).

The estimated ratios of overlap factors $OR_R$ and $OR_Q$ are plotted in Figure 11 b) and c), at 7.5 m resolution (thin line) and after smoothing (thick line, final correction used hereafter). Peak divergence is 5 to 7%, at ~150 m. Convergence within 1% happens at ~400 m, but oscillations of lower amplitude persist until ~3 km. We note that for $OR_Q$, deviations do not exceed the ±0.7% required to maintain bias below 1°C. They are nevertheless corrected.

4.3 Comparison to radiosoundings and calibration, estimation of residual error

12 nighttime and 24 daytime radiosoundings were launched from Trappes between May 20th and June 2nd, 2020. Lidar profiles are averaged from 0 to 40 minutes after the radiosounding launch time. The range averaging is progressive and defined to keep the night time temperature error below 1.5°C: range bins are 15 m long below 100 m agl, growing to 360 m above 8 km agl.

In order to debias WVMR and temperature measurements from residual errors on $OR_R$ and $OR_Q$, we perform a three-step calibration:

- First step: we exclude the first 1500 m agl of the profiles when fitting $rH_2O$ in-situ vs $R'$ and $Q'$ vs $T$ in-situ to estimate $K$ and $f$ respectively. This initial calibration is shown in Figure 12 a) & d).

- Second step: using these first estimates, we then plot the ratios between the lidar observables $R'$ & $Q'$ and the expected observables deduced from the in-situ measurements and these initial calibration parameters. This provides an estimate of the remaining biases on $OR_R$ and $OR_Q$, which we find to be up to ~4% and ~1.8% respectively. This represents a small correction to the overlap ratios estimated while shooting horizontally, but remains larger than the requirements of precision specified in Table 1. The modelled corrections of $OR_R$ and $OR_Q$ are plotted in red in Figure 12 b) & e). We fit a sum of three exponential falls to the mean, of the form: $1 + a_1 \exp(-z/z_1) + a_2 \exp(-z/z_2) + a_3 \exp(-z/z_3)$, with $a_i$ coefficients and $z_i$ ranges to be adjusted.

- Third step: we apply the previous estimates of $OR_R$ and $OR_Q$ and we perform a new calibration using all the data (down to 200 m agl), yielding more precise estimates of calibration constants, as shown in Figure 12 c) & f).
In the three steps, data with SNR lower than 10 for $R'$ and 30 for $Q'$ are rejected so as to limit the impact of noise present at higher altitudes.

Figure 12. Results of calibration on 12 nighttime and 24 daytime radiosoundings launched from Trappes between May 20th and June 2nd, 2020 for WVMR (upper row) and temperature (lower row), in three steps: calibration on measurements above 1500 m (a/d) with samples as crosses (one color per radiosonde) and calibration curve in black; residual overlap ratio estimation (b/e) with samples as crosses, mean ratio in blue, random error on mean ratio as vertical bars, and model in red; calibration on all results (c/f). Daytime samples are limited to SNRs above 10 for $R'$ (WVMR) and 30 for $Q'$ (temperature).

The reliability of this calibration along time has been tested by comparing to the same exercise performed two months later at the end of July 2020. After calibration in the same conditions than in May, we found $K$ decreased by ~7.3%, and the temperature associated to a given value of $Q'$ to be ~2.1°C higher. However, $OR_R$ and $OR_Q$ were still accurate within the reachable precision, i.e. ~0.2%. It was later proven that a malfunction of the laser seeder was responsible for a slow drift of the emitted wavelength. Thus, although a regular verification of the calibration is necessary, the measurement of the overlap ratios is reliable.
Figure 13. Residual deviations between lidar and Trappes radiosoundings in terms of WVMR, temperature and relative humidity, for night time (a/b/c) and daytime (d/e/f), with mean deviation (thick lines), and RMS error (colored rectangles). The error corresponding to noise levels on the lidar signal is shown as darker rectangles. Cloudy profiles have been discarded.

Daytime measurements are limited to SNRs above 5 for $R$ (WVMR) and 20 for $Q$ (temperature).

In Figure 13, we examine the residual deviations between the lidar and the same series of radiosoundings used for the calibration. RH has been derived using Eq. (14) from lidar-estimated WVMR and temperature, and the pressure profile given by radiosoundings. For each parameter $r_{H2O}$, $T$ and $RH$, we plot for daytime and night time profiles the mean and RMS deviations averaged over large range bins as colored bars, as well as the propagated signal error as darker shaded areas. This allows to compare the observed random error to what could be expected from the level of noise on the lidar measurements. Note that only profiles with good SNR unperturbed by clouds have been selected for this comparison.
On WVMR, the results show little bias, and RMS deviation is dominated by spatial atmospheric variability at night and at low altitude (when SNR is high), and by lidar noise in all other cases. On temperature, most of the RMS deviation is explained by noise; a ~1°C significant bias is still seen below 800 m. This could be due in part to an underestimated correction of ORQ (only ~0.8%) due to the regularized model used to approximate it, but also to local effects. On Figure 13 c) and f) are plotted the consequences of this bias on relative humidity \( RH \) to be around 2 to 4%RH, but also the resulting error to be expected. We see that with the defined averaging, random error is around 2% RH up to 5 km agl during nighttime and 1 km agl during daytime, growing fast above.

Table 4. Statistics of observed differences for \( n_{H2O} \), \( T \), and \( RH \): experimental Mean Differences (MD), Root-Mean Square Differences (RMSD), averaged over two different range bins, in the low troposphere (1-2 km) and the free troposphere (5-6 km). Comparison to the “natural” atmospheric variability between the lidar and RS sites as modelled by the ECMWF/IFS ERA5 reanalyses (difference over the considered period between grid points nearest to each of the two sites), and to the theoretical root-mean-square error (RMSE) derived from the variance of the RR signals. The grid points are located 8 km WNW of the lidar and 2 km S of the RS launching station respectively, 18.3 km apart, and almost all RS trajectories below 6 km altitude are contained within the same “pixel” of the ERA5 fields as the RS station.

|            | Range resolution \( \Delta z \) | Model atmos. MD (night/day) | Experimental MD (night/day) | Model atmos. RMSD (night/day) | Theo. RMSE (night/day) | Experimental RMSD (night/day) |
|------------|---------------------------------|------------------------------|-----------------------------|-------------------------------|------------------------|-------------------------------|
| **WVMR**   | 1-2 km 84 m                     | -0.03                        | +0.06/-0.05                 | 0.41                          | 0.03/0.4               | 0.54/0.65                     |
|            | 5-6 km 168 m                    | \(<10^2\)                    | -0.07                       | 0.11                          | 0.04                  | 0.15                          |
| **Temperature** | 1-2 km 84 m               | +0.15                        | +0.25/+0.3                  | 0.33                          | 0.4/0.7               | 0.6/0.7                       |
|            | 5-6 km 168 m                    | +0.05                        | +0.4                        | 0.28                          | 0.75                  | 0.95                          |
| **Relative humidity** | 1-2 km 84 m     | -0.23                        | +0.8/-0.5                   | 6.37                          | 1.7/5.5               | 6.5/10                        |
|            | 5-6 km 168 m                    | -0.70                        | -3.3                        | 7.52                          | 2.2                   | 7                             |

To support the above interpretation, in Table 4 we compare the experimental mean difference and RMS difference plotted on Figure 13, averaged over two altitude ranges (low troposphere,
LT, 1 to 2 km, and free troposphere, FT, 5 to 6 km), to i) the natural variability of the atmosphere between the radiosondes at Trappes and the lidar at LSCE, as modelled by ERA5 reanalyses of the ECMWF/IFS weather model, ii) the expected random error given the noise level on the RR signals. Nighttime and daytime values are indicated in the LT, only nighttime values in the FT.

We see that the experimentally observed values of RMSD are rather consistent with the quadratic sum of the RMS variability of the atmospheric variables between Trappes and LSCE, and of the noise-induced RMS error. The excess random difference is thus well explained by the distance. There is still a discrepancy with the mean difference of temperature however; it is not fully explained by the differences of temperature at the locations of the two profiles seen in ERA5. The model used to approximate the correction may be imperfect, and introduce small errors when the necessary correction is large and fast-varying. We aim to improve this in the future by a better estimation the overlap ratios horizontally, for instance using a large folding mirror instead of tilting the lidar, which induces varying mechanical constraints on the optics. This should greatly reduce the necessary correction function and the remaining error should be limited by the horizontal inhomogeneity of the atmospheric temperature over a few kilometers.

5 Conclusion

During the qualification of the rotational Raman channels for the WALI lidar of LSCE, with the aim of providing profiles of relative humidity, we encountered important sources of bias that are seldom described in the now abundant literature involving such systems. We highlighted the predominant effects of the dependency of filter transmittance and detector sensitivity upon angle of incidence and point of impact, respectively. Because the latter parameters are directly proportional to field angle, they cause range-dependent biases on the RR/VR signal ratios that are several times greater than the required accuracy of lidars for temperature measurements (only 0.79% for 1°C here), less so for water vapor measurements. We established that this effect cannot be suppressed by using fiber optics between the receiver and polychromator, because scrambling of the lidar field of view does not happen radially in the fiber. Mitigation efforts impose the careful alignment of each filter at normal incidence to the input beam, and the verification of the spectral transmittance of each channel on a spectrometer. The thermal stability of the polychromator is also of prime importance. Other significant bias sources include electro-magnetic perturbations of signal baselines and PMT gain variation, which must be mitigated. The impact of fiber optics fluorescence, and of the measured laser linewidth or short-term wavelength drift were shown to be negligible in the WALI system.
After a measurement of RR/VR channel ratios during horizontal shots, which showed the significant impact of the above phenomena (up to 5% bias on ratios below 300m, ~1% higher), we calibrated and de-biased the WALI measurements using radiosondes launched from the nearby Trappes station of Météo-France. Between the de-clouded lidar measurements and the radiosonde profiles, the remaining mean differences are small (below 0.1 g/kg on water vapor, 1°C on temperature) and RMS differences are consistent with the expected error from lidar noise, calibration uncertainty, and horizontal inhomogeneities of the fields between the lidar and radiosondes. On relative humidity we thus reach a goal of ~10%RH random error and 5%RH systematic error up to 9 km by night and 1.5 km by day, with 40 min time integration and progressive vertical integration of 15 to 360 m at 10 km. The systematic error on RH is dominated by bias on temperature, whereas the random error is dominated by noise on water vapor measurements.

Thus exhaustively qualified, the WALI system may be applied in the near future to exercises assimilating thermodynamic profiles in weather models, as is expected within the WaLiNeAs (Water vapor Lidar Network Assimilation experiment) project (Flamant et al., 2021). The long-term temporal evolution of Raman channel calibration, expected from various effects like differential PMT aging or laser seeder drift, induces biases variable in time over the time-scale of such a project (several months). This aspect is becoming a main focus as the community works towards operational uses of weather Raman lidars (e.g. Hicks-Jalali et al., 2020).

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