A chromium dipolar Fermi sea

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We report on the production of a degenerate Fermi gas of $^{53}$Cr atoms, polarized in the state $F = 9/2$, $m_F = -9/2$, by sympathetic cooling with bosonic $S = 3$, $m_S = -3$ $^{52}$Cr atoms. We load in an optical dipole trap $3 \times 10^4$ $^{53}$Cr atoms with $10^6$ $^{52}$Cr atoms. Despite this initial small number of fermionic atoms, we reach a final temperature of $T \simeq 0.6 \times T_J$ (Fermi temperature), with up to $10^3$ $^{53}$Cr atoms. This surprisingly efficient evaporation stems from an inter-isotope scattering length $|a_{BF}| = 85(\pm 10) a_B$ (Bohr radius) which is small enough to reduce evaporative losses of the fermionic isotope, but large enough to insure thermalization.

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There has recently been tremendous activity on dipolar quantum gases. This is due to the fact that in dipolar gases the particles interact through long-range and anisotropic dipole-dipole interactions (DDIs), which drastically changes the nature of many-body ground and excited states. After first seminal results with dipolar Bose-Einstein condensates made of chromium[1, 2], and then dysprosium[3] and erbium[4], atoms, the focus now turns towards dipolar degenerate Fermi gases, which raise fascinating prospects for the study of novel Fermi liquid properties[5], p-wave superconductivity[6], topological px+ipy phases[7], or unconventional magnetism[8–11].

Dipolar Fermi gases of dysprosium[12] and erbium[13] have recently been produced, which has enabled to observe the Fermi surface deformation induced by dipolar interactions[14]. However, the density of magnetically-tunable Feshbach resonances in these Lanthanides atoms is very large[12, 10], due to anisotropic short range interactions. As this density promises to be even higher in the context of spinor gases where more than one spin state is populated, study of magnetism might be difficult with these atoms. For this reason, chromium, with a combination of relatively strong dipole-dipole long-range anisotropic interactions and simple isotropic short range interactions, remains a unique atom for the study of the unconventional spinor properties of dipolar quantum degenerate Fermi gases.

Despite its interest, producing a dipolar Fermi gas of chromium atoms has been elusive for many years, as it represents a real experimental challenge. The main reason is the small number of $^{53}$Cr atoms that can be captured in a magneto-optical trap (MOT), at most typically $10^5$, due to relatively small natural abundance, the complex hyperfine structure, and, most importantly, the very large light-assisted loss rate in a MOT[17]. In this paper, we describe and demonstrate a way to produce quantum gases of fermionic $^{53}$Cr atoms.

Our scheme is to load in a mixture of most-abundant $^{52}$Cr atoms and minority $^{53}$Cr atoms in the same far-detuned optical dipole trap (ODT), and in performing forced evaporative cooling. Evaporative losses are smaller for $^{53}$Cr atoms than for $^{52}$Cr atoms, which results in very efficient evaporative cooling characterized by a gain of typically four orders of magnitude in phase-space density for one order of magnitude of atom losses. As a consequence, although only $3 \times 10^4$ $^{53}$Cr atoms are loaded in the dipole trap at 60 µK before evaporation, degenerate Fermi gases of up to $10^3$ atoms can be produced in less than 15 s. We analyze our evaporation scheme and are able to point out the decisive role played by the numerical value of the inter-isotope scattering length, which is smaller than the bosonic scattering length. We measure this quantity, and compare it with theoretical predictions based on mass scaling[18].

Fermi statistics leads to vanishing s-wave collisions due to Van der Walls interactions at low temperatures for polarized fermions. Therefore, evaporative cooling to degeneracy, which requires efficient thermalization, has been achieved either with a mixture of two fermionic Zeeman states[19] for which s-wave collisions are allowed, or for a Bose-Fermi mixture[20]. With dipolar species, low temperature collisions become possible even for identical fermions. This very peculiar effect due to the long range character of DDIs was first observed with Dy[12], and was used to produce the Er Fermi sea in a very efficient way[12]. However for Cr the dipolar elastic cross section is 20 times smaller than for Er, as it scales as $d^4m^2$ ($d$ being the permanent magnetic dipole, and $m$ the mass). In addition we only manage to trap in a conservative trap about 30 times less atoms than in[13], which is very unfavourable for a scenario involving only $^{53}$Cr atoms. This is why we chose to perform sympathetic cooling with the bosonic $^{52}$Cr.

We now turn to the experimental setup used in this work with special focus on the lasers. The strategy we used to Bose condense $^{52}$Cr is to accumulate atoms captured inside a MOT into a superimposed far-detuned optical dipole trap (ODT)[21]. To improve loading in the ODT we make use of optical pumping from excited $7P$ states of the MOT trapping transition to different mes-
tastable states, in which they are protected from deleterious light assisted collisions \[17\]. After the ODT is loaded, the MOT is turned off, atoms are repumped in the \(^7\)S\(_3\) ground state, optically pumped to the absolute ground state \(m_S = -3\), and finally transferred to a crossed ODT in which the evaporation is performed.

To adapt this strategy to trap both isotopes in the same ODT, new laser lines are necessary due to the hyperfine structure of the fermionic isotope. The trapping lasers needed to obtain a \(^{53}\)Cr MOT using the \(^7\)S\(_3\) \(\rightarrow\) \(^7\)P\(_4\) transition at 425 nm were reported in \[17\]. They are generated from a dedicated laser system producing 800 mW of 425 nm light. The optimal MOT for loading the ODT contains \(10^5\) \(^{53}\)Cr atoms, at a temperature of 120 \(\mu\)K, close to the Doppler temperature. Atoms decay to metastable states \(^5\)D\(_3\), \(F = 9/2\) and \(^5\)D\(_4\), \(F = 11/2\) (from excited state \(^7\)P\(_4\), \(F = 11/2\)), and \(^5\)S\(_2\), \(F = 7/2\) (from \(^7\)P\(_3\), \(F = 9/2\), see below). Repumping of these states to the ground state is performed via the excited state \(^7\)P\(_3\) \[22\].

The (horizontal) ODT is derived from a 100 W Infra Red (IR) Ytterbium fibre laser at 1075 nm. We use 60 W and control the power with an Acousto Optic Modulator (AOM). The laser is turned on and superimposed with the MOT. Frequency modulation of the AOM at fast frequency (100 kHz) allows to adapt the IR laser mode size with the MOT radius. We find the same AOM parameters for optimal loading of both isotopes.

Optimization of the loading of the IR trap with \(^{52}\)Cr was studied in \[23\]. It revealed in particular the crucial role played by the metastable \(^5\)S\(_2\) state, populated from the MOT by using a depumping beam at 427 nm (almost resonant with the \(^7\)S\(_3\) \(\rightarrow\) \(^7\)P\(_3\) transition). Optimal depumping allows to double atom number in the ODT. For the fermionic case, we could only increase the atom number by 20 % when depumping to \(^5\)S\(_2\). We interpret this reduction in efficiency as a result of significantly larger inelastic collisions between \(^5\)S\(_2\), \(F = 7/2\) \(^{53}\)Cr atoms, compared to \(^5\)S\(_2\), \(^{52}\)Cr atoms. This may arise from the non favorable "inverted" hyperfine structure in this state: energetically allowed two-body inelastic collisions processes populate the other hyperfine states of \(^5\)S\(_2\), leading to losses. We finally could accumulate about \(10^5\) \(^{53}\)Cr atoms in the ODT, to be compared with up to \(2 \times 10^6\) for \(^{52}\)Cr, with respective 1/e loading time equal to 200 (50) ms.

In our experiment, the Zeeman Slower beam used to slow down \(^{53}\)Cr substantially reduces the \(^{52}\)Cr MOT number \[17\]. Therefore, we do not load the two isotopes at the same time in the ODT. Instead we first make a \(^{53}\)Cr MOT (to load \(^{50}\)Cr atoms in the ODT), then switch off the blue beams specific for the \(^{53}\)Cr MOT and turn on the \(^{52}\)Cr MOT for a given amount of time \(\Delta t\) (to load \(^{52}\)Cr atoms in the ODT). We then detect both atom numbers, \(N_{52}\) and \(N_{53}\). As shown in Fig. 1 the presence of both isotopes in the IR trap leads to losses, attributed to inter-isotope inelastic losses \[22\]. The starting point for evaporative cooling is therefore a trade-off: when \(\Delta t\) increases, \(N_{52}\) increases, but \(N_{53}\) decreases. With \(\Delta t = 90\) ms, we obtain the following optimal mixture for evaporation: \(N_{53} = 3.1 \times 10^4\) and \(N_{52} = 1.19 \times 10^6\).

Once the atoms are optically pumped to their absolute ground state (respectively \(S = 3, m_S = -3\) and \(F = 9/2, m_F = -9/2\)), the crossed dipole trap is implemented by transferring 80% of IR power to a vertical beam, in 9 s. The total IR power is then reduced to 1 W (starting at \(t = 5\) s) in 7 s. Figure 2 shows the evolution of the Bose-Fermi temperature and atom numbers for both isotopes. Thermalization between the two isotopes is relatively good during the whole evaporation process as shown by Fig. 3. Consequently, the interspecies cross section \(\sigma_{BF}\) has to be relatively large. On the other hand, thermalization is not perfect: the fermion temperature is measured to be about 20% higher than the one of the boson. We thus infer that \(\sigma_{BF}\) is smaller than the bosonic cross section \(\sigma_{BB}\). At the end of the ramp, a \(^{52}\)Cr BEC is obtained with typically \(8 \times 10^9\) atoms, while the number of \(^{53}\)Cr atoms ranges between 500 and 1000.

The power of the IR laser is then rapidly ramped up (to 5 W) to obtain a tighter trap and freeze evaporation. Trap frequencies \(\omega_{x,y,z} = 2 \pi \times (430, 510, 350)\) Hz are measured through parametric excitation, with 5% uncertainty. In this trap, we obtain that the critical temperature for BEC is \(T_c = 380\) nK for \(10^4\) atoms, while the Fermi temperature is \(T_f = 370\) nK for \(10^3\) atoms. The experimental temperatures are obtained by fitting the velocity distributions imaged after a free fall, by a bimodal distribution for \(^{52}\)Cr, and by either \[24\] a Boltzmann or a Fermi-Dirac distribution for \(^{53}\)Cr. We obtain \(T_{52} = (180 \pm 20)\) nK and \(T_{53} = (220 \pm 20)\) nK. We therefore obtain \(T_{53}/T_f = 0.6\).

In addition to report the production of \(^{53}\)Cr degenerate gases, one of the main points of this paper is to explain
whether our strategy to reach quantum degeneracy is efficient despite the small atom number before evaporation. For that we develop the following theoretical model, based on the scaling laws for evaporation first introduced in [25]. Our main assumption is that polarized $^{53}\text{Cr}$ atoms only collide with $^{52}\text{Cr}$ atoms. This assumption is first motivated by the fact that the centrifugal barrier is of the order of 1 mK for the $p$–wave channel, much larger than the initial temperature of the cloud. As a consequence, polarized Fermions can be considered not to collide with each other through Van der Walls interactions. In addition, the expected scattering cross-section between identical Fermions due to DDIs, estimated to be $9.8 \times 10^{-18} \text{ m}^{-2}$ using first order Born approximation [26], is small enough that dipolar collisions may be neglected given the density. Therefore one can consider that fermions only collide with most abundant $^{52}\text{Cr}$ atoms. Due to large differences in atom numbers, we assume as well that evaporative losses of bosons solely come from collisions with bosons.

Given these assumptions, the rate equations for evaporation are given by:

$$\frac{dN_B}{dt} = -\sigma_{BB} n_B \bar{V} f(\eta_B) N_B - \Gamma N_B$$  \hspace{1cm} (1)

$$\frac{dN_F}{dt} = -\sigma_{BF} n_B \bar{V} f(\eta_F) N_F - \Gamma N_F$$

$$\frac{d(3N_B T_B)}{dt} = -\sigma_{BB} n_B \bar{V} f(\eta_B)(\eta_B + 1) N_B T_B - \Gamma (3N_B T_B)$$

$$\frac{d(3N_F T_F)}{dt} = -\sigma_{BF} n_B \bar{V} f(\eta_F)(\eta_F + 1) N_F T_F - \Gamma (3N_F T_F)$$

where $i = B, F$ stands for Boson of Fermion, $N_i$ is an atom number, $n_i$ a density, $\bar{V} = (16 \hbar k T / \pi m)^{1/2}$ is the mean of the magnitude of the relative velocity, $\Gamma$ is the one body loss coefficient, independently measured to be $\Gamma = 0.1 \text{ s}^{-1}$ in our experiment, $\eta$ is the ratio between the trap depth and the thermal energy, and $f(\eta) = 2(\eta - 4)e^{-\eta}$ [25, 27]. These equations assume thermal equilibrium. As noticed above the fermion temperature is slightly higher than the boson temperature, which signals a slight departure from thermal equilibrium. To interpret our data, we therefore assume thermal equilibrium for each gas, at a temperature which slightly depends on the isotope.

The first term in the right-hand side of each equation in (1) describes evaporation. One major difficulty in applying this model to quantitatively describe evaporation is that the rate of evaporation depends exponentially on $\eta$, via the exponential term in $f$. It is usually difficult to precisely measure the trap depth in one experiment (e.g. due to uncertainties in estimating waists of laser beams in situ). However, the trap depth is almost identical for the two isotopes (isotopic shifts being much smaller than the detunings of the IR laser to all optical transitions). In our analysis, we therefore strongly reduce the sensitivity to the trap depth by comparing the rate of evaporation of fermions to the one of bosons. The first two equations of (1) give:

$$\log_e \left( \frac{N_B(t_2)}{N_B(t_1)} \right) + \Gamma(t_2 - t_1) = \frac{\sigma_{BB}}{\sigma_{BF}} \frac{f(\eta_B)}{f(\eta_F)}$$  \hspace{1cm} (2)

As seen from eq. (2), the sensitivity to trap depth is not completely suppressed by the relative measurement, because the temperature of both clouds are slightly different, leading to values of $\eta_B$ and $\eta_F$ differing by up to 20 percent. We therefore first estimate the value of $\eta_B$ by comparing the measured loss rate of bosons and cooling rate. From the first and third eqs in (1) we infer:
We thus infer an agreement with the ratio of the trap depth to temperature for $a_{52-53}$ (this work), which is in good agreement with predictions based on mass-scaling. The solid line is the predicted scattering length using mass scaling of semi-classical phase [18].

An outcome of our analysis is the first measurement of $\eta_B = 6.5 \pm 0.5$, in relatively good agreement with the ratio of the trap depth to temperature $\approx 7$ which we infer from calibrating the trap depth. We thus infer $f(\eta_B)/f(\eta_B) = 2.0 \pm 0.5$.

We now use our experimental data, to estimate from eq.(2) the value for the cross-section $\sigma_{BF}$. We can use different portions of the experimental data to measure the ratio $\sigma_{BF}/\sigma_{BB}$ as shown in Fig.4. In practice, this is for example done by spanning the times $t_1$ and $t_2$ over the range of experimental times which were investigated in our experimental data. Experimental values of $\sigma_{BF}/\sigma_{BB}$ all lie in the interval $0.35 \pm 0.05$ irrespective of the choice of $t_1$ and $t_2$. This indicates that $\sigma_{BF}/\sigma_{BB}$ is insensitive to temperature to within signal-to-noise ratio. This is in good agreement with the assumptions that atoms collide mostly through $s$-wave and short-range interactions. This is also in good agreement with theoretical predictions [28].

An outcome of our analysis is the first measurement of the boson-fermion scattering length $a_{BF}$ in the $S = 6$ electronic molecular potential (both atoms being in the stretched state of lowest energy). Indeed, $\sigma_{BF} = 4\pi a_{BF}^2$ describe collisions between (distinguishable) bosons and fermions, while the value of $\sigma_{BB} = 8\pi a_{BB}^2$, which describes collisions between (undistinguishable) bosons, has been measured with accuracy [29]. In Fig.4 we report the known value of $a_6$ for $^{52}$Cr, the less-well known value for $^{50}$Cr [30], as well as our newly measured value for $|a_{BF}| = 85(\pm 0) a_B$. The good agreement with theoretical predictions based on mass-scaling [18] indicates that $a_{BF} > 0$.

Our analysis therefore confirms that $\sigma_{BF} < \sigma_{BB}$. As evaporation is optimized to be achieved as fast as possible for the boson, it is not surprising that the Fermi cloud lags slightly behind in terms of temperature. This analysis shows that our strategy to cool fermions is particularly efficient because (i) $\sigma_{BF}$ is sufficiently large to (almost) insure inter-isotope thermal equilibrium; (ii) $\sigma_{BF}$ is small enough to reduce evaporative losses of fermions, which leads to a gradual increase of the ratio of the number of fermions to the number of bosons as evaporation proceeds (see Fig.4). This increase is essential for the positive outcome of our experiment.

In conclusion, we have produced a $^{53}$Cr degenerate Fermi gas, with up to $10^4$ atoms, together with a BEC of $10^4$ $^{52}$Cr atoms. This boson-fermion degenerate mixture might have peculiar properties, due to the strong imbalance in atom numbers. The spatial mode of the Fermi sea may be deformed by strong repulsive interaction with the BEC, which is of the order of the Fermi energy. Deformation of the Fermi surface may arise as well. These effects should be amplified close to an inter-isotope Feshbach resonance.

We plan to reveal the dipolar nature of the $^{53}$C Fermi sea by studying Pauli paramagnetism at low magnetic field. Quantum statistics is expected to lead then to a very different picture than the one we obtained for $^{52}$Cr [31]. In a 3D optical lattice, $^{53}$Cr should provide a good platform to engineer new magnetism associated to XYZ spin models [3], complementary to recent studies with $^{52}$Cr [32].

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[1] A. Griesmaier, J. Werner, S. Hensler, J. Stuhler, and T. Pfau, Phys. Rev. Lett. 94, 160401 (2005)
[2] T. Koch, T. Lahaye, J. Metz, B. Fröhlich, A. Griesmaier, and T. Pfau, Nature Physics 4, 218 (2008) T. Lahaye, J. Metz, B. Fröhlich, T. Koch, M. Meister, A. Griesmaier, T. Pfau, H. Saito, Y. Kawaguchi, and M. Ueda, Phys. Rev. Lett. 101, 080401 (2008); G. Bismut, B. Pasquiou, E. Maréchal, P. Pedri, L. Vernac, O. Gorceix, and L. Vernac, Phys. Rev. Lett. 105, 040404 (2010); G. Bismut, B. Laburthe-Tolra, E. Maréchal, P. Pedri, O. Gorceix, and L. Vernac, Phys. Rev. Lett. 109, 155302 (2012)
[3] M. Lu, N.Q. Burdick, S.H. Youn, and B.L. Lev, Phys. Rev. Lett. 107, 190401 (2011)
[4] K. Aikawa, A. Frisch, M. Mark, S. Baier, A. Rietzler, R. Grimm, and F. Ferlaino, *Phys. Rev. Lett.* **108**, 210401 (2012)

[5] M. A. Baranov, M. Dalmonte, G. Pupillo, and P. Zoller *Chem. Rev.* **112**, 5012 (2012)

[6] M.A. Baranov, M.S. Marenko, V.S. Rychkov, and G.V. Shlyapnikov, *Phys. Rev. A* **66**, 013606 (2002)

[7] J. Levinsen, N. R. Cooper, and G. V. Shlyapnikov *Phys. Rev. A* **84**, 013603 (2011)

[8] D. Peter, S. Muller, S. Wessel, and H.P. Buchler, *Phys. Rev. Lett.* **109**, 025303 (2012)

[9] M. L. Wall, K. Maeda, and L. D. Carr, arXiv:1410.4226 (2014)

[10] A.W. Glaetzle, M. Dalmonte, R. Nath, C. Gross, I. Bloch, and Peter Zoller arXiv:1410.3388 (2014)

[11] D. Peter, N.Y. Yao, N. Lang, S.D. Huber, M.D. Lukin, and H.P. Buchler, arXiv:1410.5667 (2014)

[12] M. Lu, N.Q. Burdick, and B.L. Lev, *Phys. Rev. Lett.* **108**, 215301 (2012)

[13] K. Aikawa, A. Frisch, M. Mark, S. Baier, R. Grimm, and F. Ferlaino *Phys. Rev. Lett.* **112**, 010404 (2014)

[14] K. Aikawa, S. Baier, A. Frisch, M. Mark, C. Ravensbergen, F. Ferlaino *Science* **345**, 1484 (2014)

[15] A. Frisch, M. Mark, K. Aikawa, F. Ferlaino, J. L. Bohn, C. Makrides, A. Petrov, and S. Kotochigova, *Nature* **507**, 475-479 (2014)

[16] K. Baumann, N.Q. Burdick, M. Lu, and B.L. Lev, *Phys. Rev. A* **89**, 020701(R) (2014)

[17] R. Chicireanu, A. Poudreux, R. Barbé, B. Laburthe-Tolra, E. Maréchal, L. Vernac, J.-C. Keller and O. Gorceix, *Phys. Rev. A* textbf73, 053406 (2006).

[18] G. F. Gribakin and V. V. Flambaum *Phys. Rev. A* **48**, 546 (1993); V. V. Flambaum, G. F. Gribakin, and C. Harabati *Phys. Rev. A* **59**, 199 (1999)

[19] B. DeMarco and D. S. Jin, *Science* **285** 1703 (1999)

[20] A.G. Truscott, K.E. Strecker, W.I. McAlexander, G.B. Patridge, and R.G. Hulet, *Science* **291**, 2570 (2001);

F. Schreck, L. Khaykovich, K.L. Corwin, G. Ferrari, T. Bourdel, J. Cubizolles, and C. Salomon, *Phys. Rev. Lett.* **87**, 080403 (2001)

[21] Q. Beaufils, R. Chicireanu, T. Zanon, B. Laburthe-Tolra, E. Maréchal, L. Vernac, J.-C. Keller, and O. Gorceix, *Phys. Rev. A* **77**, 061601 (2008)

[22] Analysis of the loading optimization, as well as technical details of the experiment, and spectroscopic data of repumping lines, will be presented in a forthcoming paper.

[23] G. Bismut, B. Pasquiou, D. Ciampini, B. Laburthe-Tolra, E. Maréchal, L. Vernac, and O. Gorceix, *Appl. Phys. B* **102**, 1-9 (2011)

[24] For $T/T_F = 0.6$, it is expected that fitting the Fermi Dirac distribution by the Boltzmann statistics leads to the same value of temperature within 3% (B. DeMarco, PhD thesis, University of Colorado (2001)).

[25] K. M. O’Hara, M. E. Gehm, S. R. Granade, and J. E. Thomas, *Phys. Rev. A* **64**, 051403(R)

[26] S. Hensler, J. Werner, A. Griesmaier, P.O. Schmidt, A. Grütz, T. Pfau, S. Giovanazzi and K. Rzazewski *Appl. Phys. B* **77**, 765 (2003)

[27] R. de Carvalho and J. Doyle, *Phys. Rev. A* **70**, 053409 (2004)

[28] A. Simoni, private communication

[29] B. Pasquiou, G. Bismut, Q. Beaufils, A. Crubellier, E. Maréchal, P. Pedri, L. Vernac, O. Gorceix, and B. Laburthe-Tolra *Phys. Rev. A* **81**, 042716 (2010)

[30] J. Werner, A. Griesmaier, S. Hensler, J. Stuhler, T. Pfau, A. Simoni and E. Tiesinga, *Phys. Rev. Lett.* **94**, 183201 (2005)

[31] B. Pasquiou, E. Maréchal, L. Vernac, O. Gorceix, and B. Laburthe-Tolra, *Phys. Rev. Lett.* **108**, 045307 (2012)

[32] A. de Paz, A. Sharma, A. Chotia, E. Maréchal, J. H. Huckans, P. Pedri, L. Santos, O. Gorceix, L. Vernac, and B. Laburthe-Tolra, *Phys. Rev. Lett.* **111**, 185305 (2013)