Ultrafast photo-induced enhancement of electron-phonon coupling in metal-halide perovskites

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ABSTRACT: In metal-halide perovskites (MHPs), the nature of organic cations affects both, the perovskite’s structure and its optoelectronic properties. Using ultrafast pump-probe spectroscopy, we demonstrate that in state-of-the-art mixed-cation MHPs ultrafast photo-induced bandgap narrowing occurs, and linearly depends on the excited carrier density in the range from 10^{16} cm^{-3} to above 10^{18} cm^{-3}. Furthermore, time-domain terahertz (td-THz) photoconductivity measurements reveal that the majority of carriers are localized and that the localization increases with the carrier density. Both observations, the bandgap narrowing and carrier localization, can be rationalized by ultrafast (sub-2ps) photo-induced enhancement of electron-phonon coupling, originating from dynamic disorder, as clearly evidenced by the presence of a Debye relaxation component in the
terahertz photoconductivity spectra. The observation of photo-induced enhancement of electron-phonon coupling and dynamic disorder not only provides specific insight into the polaron-strain distribution of excited states in MHPs, but also adds to the development of a concise picture of the ultrafast physics of this important class of semiconductors.

Introduction

Understanding the excited carrier (photo) physics of metal-halide perovskite semiconductors is essential to unleash their optimum performance in optoelectronic applications, for instance, in light-emitting diodes and solar cells. In metal-halide perovskites Wannier-type excitons are the primary photo-generated states, since the small reduced electron mass (~0.1-0.15 $m_e$)\(^{1-2}\) and high optical relative permittivity ($\varepsilon_{opt}$~4-6.5)\(^3\) yield a Bohr radius larger than the perovskite’s lattice constant. Based on the Wannier-exciton approximation, the exciton binding energy ($R_b$) can be estimated to ~54 meV when using $\varepsilon_{opt} = 5$ in the hydrogen model\(^2\). However, $R_b$~5-15 meV was determined based on temperature-dependent measurements of the absorption spectra of the classic CH\(_3\)NH\(_3\)PbI\(_3\) (MAPbI) perovskite, analyzed in the framework of Elliot theory\(^4-6\). Such small $R_b$ can be explained when considering strong electron-phonon coupling, resulting from the perovskites’ polar ionic crystal structure, which screens efficiently the electron-hole mutual attraction potential \(^7-8\). In fact, excitons are barely observed in metal halide perovskites at room temperature (where the thermal energy $k_B T$ is ~25 meV) due to efficient thermally-assisted dissociation. Consequently, free carriers are generated by photoexcitation, indicated by the quadratic carrier-density dependence of spontaneous photon emission \(^9\).
Nevertheless, the excited carriers are not entirely free in perovskite semiconductor films. First, the carrier’s effective mobility is reduced by static disorder, caused by imperfections and thin-film inhomogeneities\textsuperscript{10,11}. Second, the perovskite’s ionic crystal lattice is soft. As a result, lattice distortions follow the motion of carriers, leading to the formation of quasiparticles known as polarons\textsuperscript{12}. Furthermore, the energetic barrier for rotation of the organic cations present in the perovskite lattice is as small as \(\sim 20\) meV\textsuperscript{13}. Consequently, the organic cations can rotate around their lattice positions at room temperature, thereby increasing dynamic disorder\textsuperscript{14}. Therefore, carriers can be scattered and trapped in localized states induced by static disorder, lattice distortions, and/or dynamic disorder\textsuperscript{15}. The intimate relation between carrier localization and dynamic disorder has been revealed by density functional theory (DFT)\textsuperscript{15-20}. It has been shown that dynamic disorder contributes to the discrepancy between the theoretically-predicted and experimentally-observed temperature dependence of polaron mobility\textsuperscript{14-15}. The latest interpretation is that carrier localization is induced by dynamic disorder, but stabilized by lattice distortion\textsuperscript{20}, or in other words, dynamic disorder is linked to polaron formation\textsuperscript{18-19}, as also observed experimentally\textsuperscript{21-22}. Since dynamic disorder scales with temperature, it enhances electron-phonon coupling and increases carrier localization at higher temperatures\textsuperscript{23}, and thereby affects the polaron formation in the perovskite bulk\textsuperscript{20}. However, the precise effect of dynamic disorder on electron-phonon coupling of excited states has remained elusive.

In this work, we employed transient absorption (TA) pump-probe spectroscopy to study electron-phonon coupling in an archetypical triple-cation perovskite film, namely FA\textsubscript{0.81}MA\textsubscript{0.14}Cs\textsubscript{0.05}PbI\textsubscript{2.55}Br\textsubscript{0.45} (FAMACs). This perovskite composition delivers a power conversion efficiency (PCE) higher than 20% in conjunction with excellent photostability in perovskite solar cells (PSCs)\textsuperscript{24-25}. Carrier density-dependent TA spectra were measured at room
temperature across carrier density ranges comparable to those observed at 1-sun illumination and above, precisely in the range from \(N \sim 3.6 \times 10^{16} \text{ cm}^{-3}\) to \(N \sim 5.8 \times 10^{18} \text{ cm}^{-3}\). We developed a model to analyze the high-energy tail of the TA spectra and revealed photo-induced bandgap renormalization (BGR). Our results demonstrate that BGR concludes in \(\sim 2\) ps and, unexpectedly, exhibits a linear dependence on the photo-excited carrier density. This linear dependence cannot be rationalized by carrier-carrier interactions, suggesting that electron-phonon coupling is its origin\(^{26}\). More precisely, for polaron formation, this anomalous BGR can only be rationalized by considering photo-enhanced electron-phonon coupling. We evidenced the presence of photo-enhanced electron-phonon coupling by time-domain terahertz (tdTHz) spectroscopy. Specifically, we find that the fluence-dependent THz photoconductivity spectra can be described by a combination of the classical Drude model and the Debye relaxation model. The Debye relaxation component in the THz photoconductivity increases with carrier density, indicating an increase of the static-dielectric response, and thus enhancement of electron-phonon coupling at high carrier densities. The stabilization of this enhancement appears to be ultrafast, because the THz photoconductivity reaches its maximum in 2 ps. Since Debye relaxation is characteristic for dynamic disorder\(^ {27}\), we ascribe the origin of the photo-enhanced electron-phonon coupling to dynamic disorder. The fraction of Drude-type carriers compared to the total number of photo-generated carriers decreases from \(\sim 10\%\) to \(5\%\) as the carrier density increases from \(N \sim 1 \times 10^{17} \text{ cm}^{-3}\) to \(N \sim 5 \times 10^{18} \text{ cm}^{-3}\), indicating that most carriers remain localized. This localization is even enhanced at high carrier densities, a consequence of increased dynamic disorder\(^ {15,20}\). Due to the low fraction of Drude-type carriers, the effective carrier mobility is about an order smaller than the expected Drude-type carrier mobility, indicating that one has to account for fraction of localized carriers, when determining effective carrier mobilities. Finally, yet importantly, we relate
the effective carrier density to the electron-phonon coupling constant and extract the photo-
enhanced fraction, which is in excellent agreement with the value predicted by linear BGR.

Our findings imply that dynamic disorder plays a major role in the physics of excited states in
perovskites. More precisely, at low-fluence, dynamic disorder increases electron-phonon coupling
and carrier localization on ultrafast timescales (<2 ps), providing polaron strain gradients that can
drive halide segregation\textsuperscript{28}. For carrier densities above a critical value, $N_c \approx 5.3 \times 10^{18} \text{ cm}^{-3}$, the
polaron strain gradients are gradually released due to spatial overlap of neighboring polarons, an
effect that can be exploited to cure light-induced halide segregation\textsuperscript{28}. Since the effective carrier
mobility decreases with carrier density, the carrier diffusion length decreases at high carrier
densities. Consequently, the tradeoff between these two effects has to be considered when
designing high performance perovskite optoelectronic devices.

**Transient absorption spectra – Analysis of the high-energy tail of the photobleach**

FAMAC films (thickness $d \approx 300$ nm) were prepared by solution-processing of FAMAC solutions
on spectroscopic-grade quartz substrates (see SI). Figure 1a shows the steady-state ground-state
absorption spectrum, analyzed in the framework of the Elliott model, assuming the absorption
(coefficient) consists of a linear combination of excitonic absorption ($\alpha_X$) and absorption of
continuum states ($\alpha_C$) as reported earlier\textsuperscript{4-6,8,29}. According to the Elliott theory, $\alpha_C$ is enhanced
by a factor $\xi$ due to Coulomb attraction between electrons and holes\textsuperscript{6}:

$$\xi(R_{b0}, x) = \frac{2\pi\sqrt{R_{b0}/x}}{1 - \exp\left(-2\pi\sqrt{R_{b0}/x}\right)}$$  \hspace{1cm} (1)
where $R_{b0}$ is the exciton binding energy, and $x = E - E_g$, where $E_g$ is the band gap. $\xi$ approaches unity when $R_{b0} \rightarrow 0$, which implies the Coulomb enhancement of $\alpha_C$ does not exist any longer once excitons are fully screened. Using $\xi$, the Elliott formula can be expressed by 6:

$$
\alpha(E) = A \frac{4\pi R_{b0}^{3/2}}{E} \delta(x + R_{b0}) + A \frac{\xi(R_{b0}, x)}{E} \sqrt{x}
$$

(2)

where $A$ is a fitting parameter related to the transfer matrix elements 29, $\delta$ is the Dirac delta function, $\sqrt{x}$ is the normalized density of states in the conduction band assuming a parabolic shape (valid below $\sim 1.82$ eV in our sample). The first term accounts for $\alpha_X$, while the second term accounts for $\xi\alpha_C$. To describe the room-temperature absorption spectra, a hyperbolic-secant broadening function accounting for thermal and inhomogeneous broadening was convoluted with Eqn. 2 (see SI), yielding $R_{b0} \sim 7.4$ meV and $E_g \sim 1.67$ eV (Fig. 1a). The decomposed $\alpha_X$ and $\xi\alpha_C$ are plotted in Figure 1a alongside $\alpha_C$. Clearly, the high-energy part of the absorption spectrum is very sensitive to $\xi$, the Coulomb screening.

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**Figure 1.** Fit of the thin film ground-state absorption spectra and of the high-energy part of the TA spectra to the Elliott model. (a) Elliott model fit to the ground-state absorption spectra of thin films. The dashed line exemplifies the continuum absorption, if excitons are fully screened ($\xi=1$). (b) High energy part of TA spectra recorded at 5 ps delay for carrier densities varying from $3.6 \times 10^{18}$ to $5.2 \times 10^{18}$ cm$^{-3}$. The pump wavelength was 475 nm ($\sim 2.61$ eV). Red lines are fits of the TA spectra between 1.72 eV and 1.82 eV to the Elliott model. Inset: a schematic of the occupational probability in the conduction band. (c) Plot of the quasi-Fermi level energy ($E_f$)
against the carrier density. The red solid line is a linear fit to $E_f$ as a function of $\log(N)$. Inset: time-dependent $E_f$ for a carrier density of $\sim 4.3 \times 10^{18}$ cm$^{-3}$.

Next, we focus on the high-energy part of the TA spectra to explore the photo-induced BGR and underlying many-body effects (Fig. 1b). When analyzing the high-energy part of the spectra, we can safely neglect photo-induced broadening. For $x$ larger than the width of the broadening function, the high-energy tails can be described by (see SI):

$$
\Delta \alpha(E) \approx A \frac{\xi(R_b, x + \Delta E_{bg})}{E} \sqrt{x + \Delta E_{bg}(1 - f_e)^2} - A \frac{\xi(R_{b0}, x)}{E} \sqrt{x} \quad (3)
$$

where $R_b$ and $\Delta E_{bg}$ are the screened exciton binding energy and the photo-induced BGR due to many-body effects, respectively. Here a positive $\Delta E_{bg}$ represents bandgap narrowing. $f_e = 1/[1+e^{(E_f-E)/k_B T_e}]$ is the Fermi-Dirac distribution function accounting for the occupation probability of electrons in the conduction band (inset in Fig. 1b), where $E_f$ is the quasi-Fermi level, $k_B$ is the Boltzmann constant, and $T_e$ is the absolute electron temperature. Since the effective mass of holes is similar to that of electrons, we assume that the occupation probability of holes in the valence band is symmetric to that of electrons in the conduction band. Compared to fits of the entire TA bleach region, Eqn. 3 only uses four fitting parameters, namely $R_b$, $\Delta E_{bg}$, $E_f$, and $T_e$, owing to the intrinsic independence of the broadening function. Using the fitting results of the ground-state absorption spectrum (see Fig. S1, $A=59451$, $R_{b0}=7.4$ meV and $E_g=1.67$ eV), the high-energy tails ($E \sim 1.72$ eV-1.82 eV) can be described very well by Eqn. 3 (Fig.1b). Here, $R_b=R_{b0}$ was used in the fitting, since even a small reduction in $R_b$ resulted in poor fits.

The time-dependent $E_f$ for $N \sim 4.3 \times 10^{18}$ cm$^{-3}$ exhibits a fast picosecond rise followed by a slow rise in the range of tens of picoseconds (inset in Fig. 1c). This is related to hot-carrier cooling limited by the phonon bottleneck. If the value of $E_f$ is smaller than $E_g$, then the electron density can be approximated by $6, 31$:
\[ N \approx 2 \left( \frac{m^* k_B T_e}{2 \pi \hbar} \right)^{3/2} \exp \left( \frac{E_f - E_g}{k_B T_e} \right) \]  

where \( m^* \) is the effective electron mass and the other parameters have been defined above or have their usual meaning. \( E_f \) mainly depends on \( T_e \) at early times when \( N \) is constant, thus its time-dependent evolution mimics the effect of hot-carrier cooling. The reason for the cooling bottleneck has been summarized recently, and it is not the focus of this work. Eqn. 4 also shows that \( E_f \) is linear in \( \log(N) \) once hot-carrier cooling has concluded (Fig. 1c).

**Dependence of BGR on photo-excited carrier density**

![Diagram](attachment:image.png)

**Figure 2. Photo-induced bandgap renormalization (BGR) in perovskites.** (a) Time-dependent BGR for a carrier density of \( \sim 4.3 \times 10^{18} \) cm\(^{-3} \). Inset: a schematic of the bandgap narrowing due to BGR. The exciton binding energy after BGR is indicated by a green double-headed arrow. (b) BGR against carrier density. The dashed line is a power law fit with \( \Delta E_{bgr} \propto N^{1/3} \). The red solid line is a fit with \( \Delta E_{bgr} \propto N \). Black arrow: the Mott density estimated from the exciton band energy. (c) Left axis: Normalized terahertz kinetics for a carrier density of \( \sim 4.3 \times 10^{18} \) cm\(^{-3} \). The green area represents the correlation (pulse width \( \sim 176 \) fs) of pump and probe laser pulses. Right axis: time evolution of electron temperature (\( T_e \)) after photoexcitation. \( T_e \) reaches its maximum soon after the instrument response (\( \sim 352 \) fs), yet the terahertz kinetics indicate a maximum at \( \sim 2 \) ps. The rise of the terahertz kinetics observed after hot-carrier cooling has concluded is an evidence of polaron formation (shaded area).

For \( N \sim 4.3 \times 10^{18} \) cm\(^{-3} \), \( \Delta E_{bgr} \) assumes a plateau between \( \sim 2-5 \) ps after reaching the maximum (Fig. 2a), indicating photo-induced BGR is concluded in \( \sim 2 \) ps. The subsequent decrease of \( \Delta E_{bgr} \)
after ~5 ps is caused by the onset of carrier recombination. The stabilized $\Delta E_{bgr}$ is ~29 meV, similar to the value extracted from MAPbI films. Since our data can only be fitted with $R_b=R_{b0}$, the nonzero $\Delta E_{bgr}$ implies that the excitonic level is red-shifted by $\Delta E_{bgr}$ (schematic in Fig. 2a). Such phenomenon cannot be explained by carrier-carrier interactions, which should leave the excitonic level virtually unchanged, because the photo-induced BGR and screening occur at the same time. We note that the formation of bi-excitons may cause a large redshift of the excitonic level. However, this is not observed here. Hence, we conclude that $\Delta E_{bgr}$ must be caused by electron-phonon interactions.

It is noteworthy that $R_b=R_{b0}$ does not imply the absence of photo-induced screening, rather the photo-induced screening occurs on longer time scales, which do not affect $R_b$. This time scale can be estimated by $t_{scr}>R_{b0}/\hbar$, where $\hbar$ is the Planck constant, yielding $t_{scr}>554$ fs. Despite $t_{scr}$ larger than the time resolution of our TA spectroscopy setup (~176 fs), stabilized excitons are hardly detected due to very efficient thermal dissociation. In the framework of the hydrogen model, the effective exciton dielectric response ($\varepsilon_X$) at the ground state can be evaluated by: $R_{b0}=13.6 m_r/(m_e \varepsilon_X^2)$ eV, where 13.6 is the Rydberg constant and $m_r$ is the reduced electron mass. Here we obtain $\varepsilon_X \sim 14.85$ when using $m_r=0.12 m_e$ (ref. 1-2). According to the Mott transition criterion of $a_B/\lambda_D=1.19$, where $a_B=0.0592 m_e \varepsilon_X/m_r$ is the effective Bohr radius of the exciton and $\lambda_D=[\varepsilon_X E_T/(8 \pi^2 N)]^{1/2}$ is the Debye screening length, using the thermal energy $E_T \sim 25$ meV at room temperature, the estimated Mott density in our sample is $N_{Mott} \sim 2 \times 10^{16} \text{ cm}^{-3}$ (Fig. 2b), indicating, hot excitons are separated instantaneously by phonon scattering if $N>2 \times 10^{16} \text{ cm}^{-3}$.

The stabilized value of $\Delta E_{bgr}$ plotted versus the carrier density is shown in Figure 2b; likewise, the dependence cannot be explained by carrier-carrier interactions. In fact, in a doped semiconductor where carrier-carrier interactions are dominant, BGR should follow a power law.
dependence on the carrier density according to: \( \Delta E_{bgr} \propto N^k \), where \( k \sim 1/3 \), when electron-defect scattering is not significant \(^{37-38}\). However, Figure 2b shows \( k \sim 1 \) in our sample, which cannot be explained by carrier-carrier interactions. The same results are found in other mixed-cation perovskites (see Fig. S2). The \( k=1 \) dependence can also result from electron-phonon interactions. Perovskites are polar materials and their static-dielectric responses (\( \varepsilon_s \)) are much larger than the optical ones (\( \varepsilon_{opt} \)) \(^3,14\), resulting in pronounced Fröhlich electron-phonon coupling according to:

\[
a_{ep} = \frac{1}{137} \sqrt{\frac{m^* c^2}{2\Omega_{LO} \varepsilon_{opt}}} \left( \frac{1}{\varepsilon_{opt}} - \frac{1}{\varepsilon_s} \right) \tag{5}
\]

where \( 1/137 \) is the fine structure constant, \( c \) is the speed of light, and \( \Omega_{LO} \) is the effective beating energy of longitudinal optical (LO) phonons. \( a_{ep} \sim 1.8-3.2 \) is obtained for the ground state when using \( \varepsilon_{opt} \sim 4-6.5 \) (ref. 3), \( \varepsilon_s \sim 35 \) (ref. 3), \( \Omega_{LO}/\hbar \sim 3.7 \) THz (ref. 36), and \( m^* = 0.23 m_e \) (ref. 27), yielding a bandgap narrowing of \( E_{pol} \sim a_{ep} \Omega_{LO} = 27.3-48.3 \) meV, induced by the electron polaron formation \(^{40}\). The narrowing is expected to double when hole polarons are also involved \(^{40}\). While we have no clear evidence of polaron formation, indirect evidence is found when comparing the hot-carrier cooling with the rise of the time-resolved terahertz signal. Figure 2c shows that the terahertz photoconductivity has reached only half of its maximum when hot-carrier cooling has concluded, indicating electron-phonon interactions are the main reason for the rise in the first 1-2 ps. This phenomenon has been ascribed unambiguously to polaron formation in single-cation perovskites \(^{41}\).

Generally, \( E_{pol} \) does not contribute to \( \Delta E_{bgr} \), because it is contained in the ground-state absorption spectrum from which \( E_g \) is extracted (Fig. 1a). However, if \( a_{ep} \) is enhanced by photoexcitation, \( E_{pol} \) can contribute to \( \Delta E_{bgr} \) according to:

\[
\Delta E_{bgr} \sim 2a_{ep} \Omega_{LO} \tag{6}
\]
This enhancement can be enabled by the presence of coupling between photon-induced dynamic disorder and the lattice distortion \(^{21,22}\).

**Photo-enhanced dielectric response**

The photo-enhanced dielectric response was first revealed by electrical experiments \(^{42,43}\), however, the conclusions have remained debated \(^{44}\). Here we provide further evidence based on tdTHz spectroscopy. Following the measurement of the tdTHz spectrum without prior photoexcitation \((E_{THz})\), the photo-induced tdTHz spectra \((\Delta E_{THz})\) were recorded at 5 ps after photoexcitation (inset in Fig. 3a). The differential tdTHz spectra in the frequency domain \((\Delta E_{THz}/E_{THz})\) can be obtained by Fast Fourier Transformation (FFT), and subsequently the photo-induced change of the dielectric response \((\Delta \varepsilon_{THz})\) can be calculated by \(^{45}\):

\[
\frac{\Delta E_{THz}}{E_{THz}} = -\frac{1}{\varepsilon_0 c (1 + n_{sub})} \int_0^d \Delta \sigma(\omega, x) dx, \quad \Delta \varepsilon_{THz}(\omega) = \frac{i\Delta \sigma(\omega)}{\omega \varepsilon_0}
\]

where \(\varepsilon_0\) is the vacuum dielectric constant, \(c\) the speed of light, \(n_{sub} \approx 2.13\) the refractive index of the quartz substrate in the terahertz region, \(d\) is the sample thickness, \(\Delta \sigma\) the photo-induced change of the photoconductivity, and \(\omega\) is the angular frequency.
Figure 3. Photo-induced change of terahertz photoconductivity. (a) The photo-enhanced dielectric response in the terahertz region. Inset: the photo-induced change of the terahertz electric field recorded at 5 ps after photoexcitation for carrier densities varying from $1 \times 10^{17}$ to $5 \times 10^{18} \text{ cm}^{-3}$. The pump wavelength was 550 nm (~2.25 eV). (b) The real part of the photo-induced change of the terahertz photoconductivity. Red solid lines are fits using a combined Drude model and Debye relaxation model (DD model). Blue solid lines are the Drude components. Shaded areas represent the Debye relaxation components. (c) The imaginary part of the photo-induced change of the terahertz photoconductivity (stacked for clarity, dashed lines are zero lines). Red solid lines are fits to the DD model, dash-dotted lines are fits to the Drude-Smith model (DS model).

Figure 3a shows the real part of $\Delta \varepsilon_{\text{THz}}$ increases with carrier density, especially at low frequencies. This behavior is similar to the dielectric model of Debye relaxation related to dynamic disorder:

$$\varepsilon(\omega) = \varepsilon_{\text{opt}} + \frac{\varepsilon_s - \varepsilon_{\text{opt}}}{1 - i\omega \tau_r}$$  \hspace{1cm} (8)$$

where $\varepsilon_s$ is the static dielectric constant and $\tau$ is the Debye relaxation time. $\tau$ is related to the phonon activation energy ($E_a$) and the thermal energy by $\tau = \tau_0 \exp(E_a/E_T)$ with constant $\tau_0$. Since $E_T$ is determined by the lattice temperature, which does not change significantly, $\tau$ can be considered constant in our experiments. Eqn. 8 implies that dynamic disorder contributes to $\Delta \varepsilon_{\text{THz}}$.

More precisely, the photo-induced low energy polarizations give rise to the dielectric response.

Next, we turn to the complex photoconductivity change $\Delta \sigma$, which is shown frequently in THz works (Fig. 3b-3c). At low carrier densities, $\Delta \sigma_1$ (the real part of $\Delta \sigma$) is virtually frequency independent (Fig 3b) and $\Delta \sigma_2$ (the imaginary part of $\Delta \sigma$) is close to zero (Fig. 3c). These spectral signatures indicate, the photoconductivity is mediated by free charges that undergo high rate scattering events. At high carrier densities, $\Delta \sigma_1$ drops at the low frequency side and $\Delta \sigma_2$ shows a zero-crossing. Such behavior has been explained in the framework of the Drude-Smith model (DS model) which involves carrier localization.
\[
\Delta \sigma(\omega) = \frac{e^2}{m^*} \frac{N_D \tau_{sc}}{1 - i\omega \tau_{sc}} \left[ 1 + \sum_{j=1}^{\infty} \frac{c_j}{(1 - i\omega \tau_{sc})^j} \right]
\]  

(9)

where \(e\) is the unit charge of electron, \(N_D\) is the density of Drude carriers, \(\tau_{sc}\) is the carrier’s momentum scattering time. \(c_j\) is a parameter (-1\(\leq c_j \leq 0\)) that accounts for photoconductivity renormalization caused by the \(j\)-th scattering event. Here, the scattering time for each scattering event is considered unchanged. \(c_j=-1\) implies full back scattering (no conduction), while \(c_j=0\) implies no backscattering (Drude conduction). A negative \(c_j\) shifts the Drude response to high frequency.

The DS model fits well at low carrier densities, however, it cannot describe \(\Delta \sigma_2\) at high carrier densities (Fig. 3c), indicating localized carriers exhibit different scattering times due to dynamic disorder. Since \(\Delta \sigma_2\) is directly related to the real part of \(\Delta \varepsilon_{THz}\) (Eqn. 7), we combined the Drude model and Debye relaxation model (DD model) to describe our data:

\[
\Delta \sigma(\omega) = \frac{e^2}{m^*} \frac{N_D \tau_{sc}}{1 - i\omega \tau_{sc}} - \frac{i\varepsilon_0 \omega \Delta \varepsilon_s}{1 - i\omega \tau_r}
\]

(10)

where \(\Delta \varepsilon_s\) is the photo-induced change of the static dielectric response originated from dynamic disorder. The first term on the right side of the equation accounts for the Drude photoconductivity, the second term accounts for the photoconductivity resulting from dynamic disorder. \(\Delta \sigma_1\) and \(\Delta \sigma_2\) can be well fitted globally by the DD model (Fig. 3b-3c), with \(\tau_{sc} \sim 16.7\) fs and \(\tau_r \sim 343\) fs. The shaded area in Figure 3b represents the photoconductivity originating from dynamic disorder, which tends to become zero at \(\omega=0\), indicating dynamic disorder does not support long range photoconductivity.

Discussion
The fraction of Drude carriers among all photo-generated carriers \((N_D/N)\) is shown in Figure 4a (top panel), alongside the ratio of \(\Delta \varepsilon/ N\) (bottom panel in Fig. 4a). We find that \(N_D/N\) is only \(\sim5\%-10\%\) depending on the carrier density, similar to the value determined for MAPbI films \(10\) and MAPbI single crystals \(47\). \(\Delta \varepsilon/ N\) is almost constant, indicating a linear increase of \(\Delta \varepsilon\) as carrier density increases. However, the uncertainty is significant at low carrier densities, because of the poor signal-to-noise ratio. To confirm that \(N_D/N\) and \(\Delta \varepsilon/ N\) do not change significantly at low carrier densities, the effective carrier mobility \((\mu_{\text{eff}})\) was calculated by \(\mu_{\text{eff}}=\mu N_D/N\) (Fig. 4b), where \(\mu\) is the mobility of Drude carriers: \(\mu=e \tau_{\text{sc}}/m^*\sim127.8\ \text{cm}^2/\text{V/s}\). For comparison, the effective mobility was also directly calculated from the frequency-averaged \(\Delta \sigma\) by \(\mu=\sigma_{\text{avg}}/Ne\) (Fig. 4b). We expected that \(\mu_{\text{\sigma}}>>\mu_{\text{eff}}\) if \(N_D/N\rightarrow1\) at low carrier densities, however, Figure 4b shows \(\mu_{\text{\sigma}}\) is only slightly larger than \(\mu_{\text{eff}}\) for all carrier densities investigated, indicating that there is no significant change of \(N_D/N\) and \(\Delta \varepsilon/ N\) at carrier densities around \(N\sim10^{17}\ \text{cm}^{-3}\). The low value of \(N_D/N\) indicates \(\mu_{\text{eff}}\) mainly originates from a small fraction of photo-generated carriers, consistent with the complicated localization nature in MHPs \(15\). Our finding also suggests that \(\mu_{\text{\sigma}}\) is a good approximation of \(\mu_{\text{eff}}\) without the need to extract it from fits of the terahertz photoconductivity.
Figure 4. Carrier localization and effective carrier mobility in FAMACs films. (a) Top panel: The fraction of Drude carriers among all the photo-generated carriers. Bottom panel: Photo-induced change of static dielectric response, scaled by carrier density. The dashed line indicates $\Delta \Delta \epsilon/N=2.6 \times 10^{-18}$ cm$^3$. (b) The effective carrier mobility obtained from the momentum scattering time (open circles) and the averaged photoconductivity (filled circles), respectively. The red solid line is a polaron mobility fit (Eqn. 11). (c) Photo-enhanced electron-phonon coupling ($\Delta a_{ep}$) obtained from TA spectra (open squares) and terahertz photoconductivity (pink area), respectively. Red solid lines are the upper limit and lower limit of $\Delta a_{ep}$, calculated by using different optical dielectric response ($\epsilon_{opt}$). Red line: $\epsilon_{opt}=4$. Black line: $\epsilon_{opt}=6.5$. (d) Polaron strain gradients
evaluated by the volume ratio of polarons (see Eqn. 12 in the main text). The critical carrier density is indicated by black arrow. Red line: $\varepsilon_{\text{opt}}=4$. Black line: $\varepsilon_{\text{opt}}=6.5$.

Figure 4a shows $ND/N$ decreases with carrier density, indicating photo-enhanced carrier localization. The localized carriers likely form large polarons. While ‘polaronic excitons’ may exist at room temperature, if the carrier density is sufficiently low ($\sim 10^{16}$ cm$^{-3}$) or if the exciton binding energy is high ($\sim 200$ meV), stabilized excitons are unlikely to be present in our experiments (Fig. 2b). The enhanced carrier localization coincides with the increase of the shaded area in Figure 3b, confirming the intimate relation between carrier localization and dynamic disorder. Since a positive $\Delta\varepsilon$ will result in an increase of $a_{ep}$ (Eqn. 5), in the weak-coupling regime, $\mu_{\text{eff}}$ can be related to $\Delta a_{ep}$ by using the concept of polaron mobility:

$$
\mu_{\text{eff}} = \mu_0 \left( \frac{a_{ep0}(1 + a_{ep0}/6)}{(a_{ep0} + \Delta a_{ep})(1 + a_{ep0}/6 + \Delta a_{ep}/6)} \right)
$$

where $\mu_0$ and $a_{ep0}$ are the polaron mobility and Fröhlich electron-phonon coupling constant at $N \to 0$, respectively, and the term $1+a_{ep0}/6$ indicates the polaron mass is enhanced by a factor of $\sim a_{ep}/6$ compared to the effective electron mass in the rigid lattice. Combining Eqn. 5 and Eqn. 11, only three unknown parameters remain: $\Omega_{LO}$, $\varepsilon_{opt}$ and $\varepsilon$. For simplicity, we fit $\mu_{\text{eff}}$ by using $\Delta\varepsilon/N=2.6 \times 10^{-18}$, $\Omega_{LO}/\hbar=3.7$ THz, and $\varepsilon_{opt}=4-6.5$ (Fig. 4b). The fitted $\varepsilon$ is $\sim 9-12.6$, much smaller than the theoretically predicted value. The discrepancy can arise from the uncertainty of $\Omega_{LO}$ and because electron-phonon coupling is primarily mediated by optical phonons, which only contribute weakly to the static dielectric response.

With $\Delta\varepsilon=2.6 \times 10^{-18}$, $\Omega_{LO}/\hbar=3.7$ THz, $\varepsilon_{opt}=4-6.5$ and $\varepsilon=9-12.6$, $\Delta a_{ep}$ is calculated and plotted in Figure 4c, in good agreement with the $\Delta a_{ep}$ estimated from the TA experiments by Eqn. 6. As $\Delta\varepsilon$ was assigned entirely to optical phonons in the fit (Fig. 4b), the good agreement indicates
dynamic disorder is strongly coupled with lattice distortion, consistent with recent reports 21-22. The coupling time is ultrafast (<2 ps, see rise in Fig. 2c) and related to the Debye relaxation time $\tau_r \sim 343$ fs. Since $\Delta a_{ep}$ is only determined by the carrier-density dependence of the dynamic disorder, its value is marginal at carrier densities below $N \sim 10^{17}$ cm$^{-3}$ (Fig. 4c), indicating $\Delta a_{ep}$ can be neglected for MHP solar cells that work under 1-sun illumination. However, $\Delta a_{ep}$ exacerbates the polaron strain gradients and thereby the halide segregation 28. Under high irradiance, $\Delta a_{ep}$ reduces the carrier mobility and thus the carrier diffusion length.

Next, we use the volume ratio of polarons to evaluate the polaron strain gradient ($g_{pol}$). We note that, when two adjacent polarons merge, the polaron strain cancels in the overlapping part:

$$g_{pol} \sim \min \left[ \frac{r_{pol}^3}{d_{pol}^3}, \frac{(d_{pol} - 2r_{pol})^2}{d_{pol}^3} \right]$$  \hspace{1cm} (12)

where $r_{pol}$ is the Feynman polaron radius, 52 and $d_{pol}$ is the distance between two neighboring polarons. The two can be approximated by:

$$r_{pol} = \hbar \sqrt{\frac{3v^{-1}}{2m_e(v^2 - w^2)\Omega_{LO}}} \quad d_{pol}^3 \approx \frac{1}{N}$$  \hspace{1cm} (13)

where $v=3+2a_{ep}/9$ and $w=3$ are variable parameters in units of $\Omega_{LO}$. 52 The calculated $r_{pol}$ and $d_{pol}$ are given in SFig. 3, and $g_{pol}$ is plotted in Fig. 4d. When the carrier density increases, $g_{pol}$ reaches its maximum at a critical carrier density of $N_C \sim 5.3 \times 10^{18}$ cm$^{-3}$. When $N > N_C$, $g_{pol}$ drops due to the spatial overlap of adjacent polarons. Therefore, high irradiance can be used to cure light-induced halide segregation and to alter the perovskite bandgap 28.

In conclusion, triple-cation-mixed MHP films (FAMACs) were investigated by TA spectroscopy and tdTHz spectroscopy. We developed a model to analyze the high-energy tails of the TA spectra, taking into account the exciton binding energy and the photo-induced BGR. We
demonstrate that the photo-induced BGR reveals ultrafast (<2 ps) photo-enhanced electron-phonon coupling, which has its origin in dynamic disorder, as evidenced by the Debye relaxation component observed in the terahertz photoconductivity spectra. Furthermore, we determined that photo-generated carriers are highly localized. Importantly, the effective carrier mobility can be approximated from the frequency-averaged terahertz photoconductivity measurements without further fits. Finally, we extracted the photo-enhanced electron-phonon coupling constant as a function of the carrier density, and we revealed ultrafast coupling (<2 ps) between dynamic disorder and the lattice distortion. Our findings provide insights into the ultrafast photophysics of perovskites, specifically the polaron strain distribution of excited states in perovskite devices and as a function of the photogenerated carrier density.

AUTHOR INFORMATION

The authors declare no competing financial interests.

AUTHOR CONTRIBUTIONS

M.W. performed the time-domain terahertz measurements and data analysis. He conceived and developed the theoretical model and wrote the initial draft of the paper. Y.G. performed the ground-state absorption and transient absorption measurements. K.W. prepared the perovskite thin film samples. S.D.W. and F.L. supervised the work and revised the manuscript. All authors contributed to refining the final version of the manuscript.

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Supplementary Information

Ultrafast photo-enhancement of electron-phonon coupling in an organometal halide perovskite film

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Figure S1: Elliott fitting to the ground-state absorption spectra. The inset tables list the fitting results obtained with two different broadening functions: Voight distribution and hyperbolic-secant distribution.

FAMACs: $\text{Cs}_{0.05}(\text{FA}_{0.83}\text{MA}_{0.17})_{0.95}\text{Pb(I}_{0.83}\text{Br}_{0.17})_3$

FAMARb: $\text{Rb}_{0.05}[(\text{FA}_{0.83}\text{MA}_{0.17})_{0.95}\text{Pb(I}_{0.83}\text{Br}_{0.17})_3$

FAMA: $(\text{FA}_{0.83}\text{MA}_{0.17})\text{Pb(I}_{0.83}\text{Br}_{0.17})_3$
Figure S2: Photo-induced bandgap renormalization extracted from the high energy tails of the TA spectra for different perovskite films. Solid lines are linear fits to the data, respectively.
Figure S3: Polaron radius ($r_{pol}$) and the distance between two neighboring polars ($d_{pol}$) at different carrier densities, calculated using Eqn.13 in the main manuscript.
Section 1. Materials and Sample Preparation

Materials: PbI₂ and PbBr₂ were purchased from TCI. FAI and MABr were purchased from Dyesol. CsI, RbI and all anhydrous solvents (DMF, DMSO, chlorobenzene) were purchased from Sigma-Aldrich. SnO₂ colloid precursor was obtained from Alfa Aesar, the particles were diluted by H₂O and isopropanol to 2.67 %. All chemicals were used without further purification. 

Perovskite film fabrication: PbI₂ (508 mg, 1.1 mmol), PbBr₂ (80.7 mg, 0.22 mmol), FAI (171.97 mg, 1 mmol) and MABr (22.4 mg, 0.2 mmol) in 1 mL of a 4: 1 (v/v) mixture of anhydrous DMF and DMSO. This resulting precursor solution for \((\text{FA}_{0.83}\text{MA}_{0.17})\text{Pb(I}_{0.83}\text{Br}_{0.17})_3\) contains a 10 mol% excess of PbI₂ and PbBr₂, respectively, which was introduced to enhance device performance. The FAMA solution was filtrated through a 0.45 μm syringe filter before use. CsI (389.7 mg, 1.5 mmol) was dissolved in 1 mL DMSO and 42 μL of the ~1.5 M CsI stock solution was added to 1 mL FAMA solution to get Cs₀.₀₅(FA₀.₈₃MA₀.₁₇)₀.₉₅Pb(I₀.₈₃Br₀.₁₇)₃ solution. RbI (318.5 mg, 1.5 mmol) was dissolved in 1 mL of DMSO and 42 μL of the ~1.5 M RbI stock solution was added to 1 mL FAMA solution to yield Rb₀.₀₅[(FA₀.₈₃MA₀.₁₇)]₀.₉₅Pb(I₀.₈₃Br₀.₁₇)₃ solution. For the solar cell performance please see Ref. 53 in the main article.

Section 2. Ground-state Absorption Coefficient

Ground-state absorption measurements were performed using a PerkinElmer Lambda 950 UV/Vis/NIR spectrophotometer. To reduce the impact of reflection on the absorption spectra, the absorption coefficient was calculated by:

\[
\alpha(E) = -\frac{1}{d} \log \left( \frac{T}{1-R} \right)
\]

where \(d\) is the sample thickness, \(R\) is the reflectivity, and \(T\) is the transmissivity.

Section 3. Transient Absorption (TA) Spectroscopy

Our TA setup uses a commercial Ti:sapphire amplifier operating at 800 nm with a repetition rate of 3 KHz as laser source. Its pulse width (FWHM) is compressed to ~125 fs. Two optical parametric amplifiers (OPA) are used to tune the laser wavelength. The white-light probe is generated by 1300 nm laser (from TOPAS1) with a CaF2 crystal that mounted on a continuously moving stage, which enables us to generate a super-continuum pulses with a spectral range from 350 to 1100 nm. The pump laser (from TOPAS2) is chopped to 1.5 KHz and delayed by an automated mechanical delay stage (Newport linear stage IMS600CCHA) from -400 ps to 8 ns. Pump and probe beams were overlapped on the front surface of the sample, and their spot sizes were measured by a beam viewer (Coherent, LaserCam-HR II) to make sure the pump beam was
about three times larger than the probe beam. The perovskite samples are stored in a nitrogen-filled chamber to protect from degradation, and photo-excited by 475 nm in this work. The probe beam was guided to a custom-made prism spectrograph (Entwicklungsbüro Stresing) where it was dispersed by a prism onto a 512 pixel complementary metal-oxide semiconductor (CMOS) linear image sensor (Hamamatsu G11608-512DA). In order to account for the reflection, we first measured the transient reflection ($R$ and $\Delta R/R$), then measured the transient absorption ($\Delta T/T$) and calculated the photo-induced change of absorption coefficient by:

$$
\Delta \alpha(E) = \frac{1}{d} \log \left( \frac{1}{1 - R} \right) - \frac{1}{d} \log \left( \frac{1}{1 - T} \right) = \frac{1}{d} \log \left( \frac{1 - \Delta T/T}{1 - \Delta R/R} \right)
$$

(S2)

Section 4. Time-resolved terahertz spectroscopy setup (TRTS)

Our TRTS setup uses the same Ti:sapphire amplifier as the TA setup. The THz emitter and detector are two 1 mm thick <110> oriented zinc telluride (ZnTe) crystals. All the THz related optics were placed in a closed chamber, which was continuously purged with pure nitrogen gas. Perovskite samples were excited by 550 nm laser pulses obtained from the TOPAS2 in the TA setup. A rotation motor mounted with a circular ND filter was used to change the pump fluence in the fluence dependent experiments.

Section 5. Determination of the carrier density

The carrier densities injected by photoexcitation were calculated by:

$$
N = F_{ph} \cdot \alpha(E_{pump})
$$

(S3)

where $F$ is the photon flux calculated by deducting the surface reflected photons from the total incident photons:

$$
F_{ph} = \frac{P \left(1 - R_{pump}\right)}{1500 \cdot \pi \cdot (D_{FWHM}/2)^2 \cdot E_{ph}}, \quad E_{ph} = \frac{hc}{\lambda}
$$

(S4)

where $P$ is the pump power. The number 1500 denotes the number of pulses that can pass the optical chopper in one second. $D_{FWHM}=3.2$ mm represents the full width at half maximum (FWHM) of the pump beam measured by the beam profiler.

The FWHM of the terahertz probe is calculated from the ratio of the maximum terahertz intensity transmitted through a 1-mm pinhole to its original intensity:

$$
\text{FWHM} = \sqrt{-\frac{\ln 2}{\ln(1 - T_{max})}} \text{ mm}
$$

(S5)
The diameter (FWHM) of the THz probe is ~1.13 mm as calculated from the measured $T_{\text{max}}$ ~42%.

Section 6. Elliott fitting to the absorption spectra

The ground-state absorption spectra were fitted by the convolution of varies broadening functions (Eqn. S8) with the following Elliott formula:

$$\alpha(E) = A \frac{4\pi R_{b0}^{3/2}}{E} \delta(x + R_{b0}) + A \frac{\xi(R_{b0}, x)}{E} \sqrt{x}$$  \hfill (S6)

where

$$\xi(R_{b0}, x) = \frac{2\pi \sqrt{R_{b0}/x}}{1 - \exp(-2\pi \sqrt{R_{b0}/x})}, \quad x = E - E_g$$  \hfill (S7)

We tried three broadening function in the fitting: Gaussian, hyperbolic-secant and Voight (Gaussian convolute with Lorentzian). Both hyperbolic-secant distribution and Voight distribution can result in perfect fitting (Fig. S1). Since hyperbolic only have one parameter, we finally choose hyperbolic-secant distribution as the broadening function for simplicity.

\[
Gaussian: G(E, \sigma) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{E^2}{2\sigma^2}\right) \hfill (S8a)
\]

\[
\text{hyperbolic-secant: } S(E, \sigma) = \frac{1}{2\sigma} \text{sech}\left(-\frac{\pi E}{2\sigma}\right) \hfill (S8b)
\]

\[
Voight: V(E, \sigma, \sigma_{lo}) = G(E, \sigma) \otimes \frac{\sigma_{lo}}{\pi E^2 + \sigma_{lo}^2} \hfill (S8c)
\]

The convolution of continuum absorption with an arbitrary broadening function is:

$$\frac{A}{E} \xi(R_{b0}, x) \sqrt{x} \otimes G(E, \sigma) = \frac{A}{E} \int_0^\infty \xi(R_{b0}, t) \sqrt{t} G(x - t, \sigma) dt$$  \hfill (S9)

When $x \gg \sigma$, the broadening function is relatively sharp, we may consider $\xi(R_{b0}, t)^{1/2}$ as slowly varying and take it out of the integration, then we have:

$$\frac{A}{E} \xi(R_{b0}, x) \sqrt{x} \otimes G(E, \sigma) \approx \frac{A}{E} \xi(R_{b0}, x) \sqrt{x}$$  \hfill (S10)

Then we can get the equation of photo-induced change of absorption shown in the main text (Eqn. 3).