ACE: Adaptive Constraint-aware Early Stopping in Hyperparameter Optimization

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Abstract
Deploying machine learning models requires high model quality and needs to comply with application constraints. That motivates hyperparameter optimization (HPO) to tune model configurations under deployment constraints. The constraints often require additional computation cost to evaluate, and training ineligible configurations can waste a large amount to tuning cost. In this work, we propose an Adaptive Constraint-aware Early stopping (ACE) method to incorporate constraint evaluation into trial pruning during HPO. To minimize the overall optimization cost, ACE estimates the cost-effective constraint evaluation interval based on a theoretical analysis of the expected evaluation cost. Meanwhile, we propose a stratum early stopping criterion in ACE, which considers both optimization and constraint metrics in pruning and does not require regularization hyperparameters. Our experiments demonstrate superior performance of ACE in hyperparameter tuning of classification tasks under fairness or under robustness constraints.

1 Introduction
When machine learning (ML) is deployed in real-world applications, practitioners desire to tune hyperparameters of a model to maximize its utility. The model is often required not only to optimize for ML objectives (e.g., accuracy, l2 loss, or F1 scores), but also to meet the deployment constraints, such as latency, storage, fairness, robustness, and explainablility. For example, when fairness is concerned, it is required to treat different demographics fairly [Perrone et al. 2021]. The constraints increase the challenge of hyperparameter optimization (HPO). If constraints are difficult to meet, we may spend high cost on ineligible trials, which violate the constraints. If constraints are expensive to compute, the step of constraint checking adds non-trivial overhead to HPO. How to early stop ineligible trials and how frequent to evaluate constraints are important factors for constrained HPO. Moreover, constraints vary in different problems in terms of constraint checking cost and difficulty to satisfy. A good solution needs to adapt to unknown constraint characteristics automatically.

We propose Adaptive Constraint-aware Early stopping (ACE), which makes use of constraint evaluation to terminate inferior trials. It decides the frequency to check constraints and the moment to stop trials to improve the efficiency of constrained HPO. We model the expected trial cost in terms of the constraint evaluation interval and provide theoretical analysis for the optimal constraint evaluation interval in the cost model. Based on the theoretical results, ACE suggests cost-effective constraint evaluation interval for each trial. Meanwhile, we propose a simple yet effective stratum truncation policy to prune unqualified trials. According to constraint evaluation results, the approach categorizes trials into groups: no-constraint-evaluation, satisfying-constraints, and violating-constraints. It termi-
Figure 1: How ACE (our method) and ASHA (Li et al., 2020) terminate two trials from random search.

'•' signifies a valid checkpoint (training iteration), satisfying the constraint, while '+' represents an invalid checkpoint, violating the constraint. ACE is a constraint-aware early stopping approach, while ASHA is a constraint-agnostic method. For Trial 1, ACE tolerates small extent of constraint violation in checkpoints 5-7 and stops it at the 28th checkpoint, close to the optimal stop point (26) for this trial. ASHA wrongly stops this promising trial in the beginning. For Trial 2, all the checkpoints are invalid. ACE can stop this infeasible trial early due to large extent of constraint violation, while ASHA keeps training it until $t = 64$. These are only two example trials to illustrate the potential advantage of using constraint information in early stopping and explain the overall empirical effectiveness of ACE even though the stop point is not necessarily optimal for every trial.

nates inferior trials of each group, which have either a relatively large extent of constraint violation or bad optimization objective. Unlike regularization methods (Xu et al., 2017), our approach does not introduce additional penalty hyperparameters. It automatically balances the goal of optimization and constraint satisfaction.

ACE is the first constraint-aware early stopping algorithm for HPO. Our experiments demonstrate that ACE obtains superior performance to constraint-agnostic early stopping baselines (Li et al., 2020), on UCI credit card dataset (Yeh and Lien, 2009) with a fairness constraint (Bird et al., 2020) and on GLUE SST2 (Wang et al., 2018) with a robustness constraint (Ribeiro et al., 2020).

2 Related work

Constrained hyperparameter optimization (HPO) uses constraint information to suggest the next candidate trials. In Bayesian optimization (Gelbart et al., 2014; Gardner et al., 2014; Bernardo et al., 2011; Perrone et al., 2021), they use additional Gaussian process to model the probability of the constraint violation. The utility function of expected improvement (EI) is multiplied by the constraint probability to suggest the next promising and feasible trials. The constraint violation can also function as a regularization term to penalize the optimization metric (Xu et al., 2017). The penalized metrics lead the optimization algorithm toward feasible regions with less violation. Since their penalty hyperparameter is sensitive to the scale of constraint violation, penalized methods require extra effort to tune the penalty. These methods check whether a trial meets or violates constraints once a trial completes training. When constraints are difficult to satisfy, we may spend unnecessary training cost on ineligible trials. Our method can examine constraints during training and stop trials without extra penalty hyperparameters.

Early stopping methods are widely applied to unconstrained HPO to reduce training time of inferior trials. Dynamic budget allocation (Li et al., 2017; 2020; Jamieson and Talwalkar, 2016) can run $N$ trials for a small budget (e.g., training iterations). They iteratively select the best $1/c$ portion and increase their budget by $c$ times. Median stopping policy (Golovin et al., 2017) stops a trial if the trial's
best optimization metric is worse than the median value of running average of all completed trials. Bandit stopping policy (Rasley et al., 2017) compares a trial’s best optimization metric to an allowable slack ratio of the global best optimization metric. Performance curve stopping policy (Swersky et al., 2014; Golovin et al., 2017; Domhan et al., 2015) use training curves of completed trials to train a regression model, which predict an optimization metric for an incoming trial. If the probability of exceeding the optimal optimization metric is low, the trial is stopped. These early stopping methods prune trials only based on the optimization metric. In the existing tuning frameworks (Liaw et al., 2018; Feurer et al., 2015) and business services (Das et al., 2020; Golovin et al., 2017), they provide classical early stopping approaches by comparing optimization metrics. No constraint information is used in their early stopping policy. We are motivated to augment these services to handle constraints required by practitioners.

3 Adaptive constraint-aware early stopping (ACE)

We present the target problem of ACE in Section 3.1, followed by our model of the trial cost with respect to the constraint evaluation interval in Section 3.2. The cost model is used to suggest cost-effective constraint evaluation interval for each trial (Section 3.3). To use both optimization and constraint metrics for pruning unqualified trials, we propose a stratum truncation policy (Section 3.4). Finally, we further optimize our method to reduce cost in constraint evaluations. (Section 3.5).

3.1 Problem statement

Given a constraint metric \( g \) and the constraint threshold \( \tau \), and the optimization metric \( \ell \), we target at finding the best feasible hyperparameter configuration \( x \in X \) with minimal computation cost. The best feasible hyperparameter configuration is defined as:

\[
\arg \min_{x \in X} \ell(x) \text{ s.t. } g(x) \leq \tau,
\]

The optimization metric could be validation loss or other metrics to minimize. We assume the values of the optimization metrics and constraint metrics change as training iterations increase (otherwise we only need to evaluate them once per trial). We also assume the constraint metric evaluation incurs non-negligible cost, and the constraint metrics are selectively evaluated at some training iterations (i.e., checkpoints). \( \ell(x) \) and \( g(x) \) correspond to the metrics at the best checkpoint among all the training iterations where these metrics are evaluated. We focus on designing an effective early stopping policy from two aspects: when to evaluate constraint metrics, and when to terminate a trial. Our early stopping policy is not tied to a particular hyperparameter search algorithm.

3.2 Expected trial cost

For a given trial, let \( C_1 \) be the constraint cost, the evaluation cost of the constraint metrics at one training iteration. Let \( C_2 \) be the primary cost, the training cost plus the evaluation cost of the optimization metric for one training iteration. We aim to reduce the total cost by choosing an appropriate constraint evaluation interval, i.e., the frequency of computing the constraint metrics. When the constraint evaluation interval is \( \beta \), the constraint metrics are computed every \( \beta \) training iterations. In other words, the constraints will be evaluated at iterations \( \beta, 2\beta, \ldots, (z-1)\beta, \) or \( z\beta \), where \( z \) is the smallest integer such that \( (z-1)\beta < T \leq z\beta \), and \( T \) is the maximal iteration of a trial. We further assume that \( p \) is the stop probability to prune a trial. For instance, if we stop a fixed percentage of inferior trials at each checkpoint, the stop probability can function as the stop probability. Then, we can formulate the expected trial cost by:

\[
E[C] = (1-p)^2[C_1 z + C_2 T] + \sum_{k=1}^{z} (1-p)^{k-1} p [C_1 k + C_2 k\beta].
\] (1)

Its first part models the cost if a trial does not stop early, while the second part models the cost of terminating a trial after \( k \) times of constraint evaluations, for \( k = 1, 2, \ldots, z \). There are \( k \) constraint evaluations in \( k\beta \) training iterations. Eq. (1) is general to any early stopping policy with linear constraint checking intervals.

We define cost ratio as \( r = C_1 / C_2 \). Then, we can simplify Eq. (1) into:

\[
E[C] = C_2 (r + \beta)^{1-(1-p)r}.
\]

The derivation is shown in Appendix A. By definition, \( z \geq \frac{T}{\beta} \). If \( z > \frac{T}{\beta} \), then we can set \( \beta' = \frac{p}{z} < \beta \).
We analyze the equation by fixing the stop probability while its right part (∀ Theorem 1). Then, we take the derivative of \( r < 1 \). If \( r > 1 \), \( \beta \) increases, and:

\[
\mathbb{E}[C|\beta] = C_2(r + \beta) \frac{1 - (1 - p)^T}{p}.
\]

### 3.3 Constraint evaluation interval

Given \( p, T, \) and \( r \), we want to obtain the optimal constraint evaluation interval \( \beta^* \) to minimize \( \mathbb{E}[C|\beta] \).

We analyze the equation by fixing the stop probability \( p = 0.5 \). First of all, we observe how max iteration \( T \) changes \( \mathbb{E}[C|\beta] \) in Figure 2 when the cost ratio \( r = 20 \). It points out that \( \beta^* \) is either 1 or \( T \) for different trials. Then, we set \( T = 16 \) to observe how \( r \) changes \( \mathbb{E}[C|\beta] \) in Figure 2. It also demonstrates that \( \beta^* \) appears in \( (1, T) \). The left part of the figure (\( r = 0.0625 \) to \( 8 \)) favors \( \beta = 1 \), while its right part (\( r = 16 \) to 1,024) prefers \( \beta = T \). The two cases both indicate that the optimal \( \beta^* \) is situated in \( (1, T) \), the two ends of \( \beta \)‘s range. We can prove Theorem 1 for general cases:

**Theorem 1.** ∀\( p, r, \) and \( T, \) the optimal \( \beta^* \) for Eq. (2) is 1 or \( T, \) i.e., \( \min_{\beta \in [1, T]} \mathbb{E}[C|\beta] \in \{1, T\} \).

If \( r < \frac{p + (1 - p)T - 1}{1 - p - (1 - p)^T} \), \( \beta^* = 1 \). If \( r > \frac{p + (1 - p)T - 1}{1 - p - (1 - p)^T} \), \( \beta^* = T \). If \( r = \frac{p + (1 - p)T - 1}{1 - p - (1 - p)^T} \), \( \beta^* = \{1, T\} \).

**Proof.** We define \( s := (1 - p)^{-1}T > 1 \) and \( T > 1 \). \( f(\beta) = (r + \beta)^{1 - \frac{s}{p} - \frac{1}{p}} \) and \( \mathbb{E}[C|\beta] \) have the same minimizers for \( \beta \in [1, T] \). We take the derivative of \( f(\beta) \):

\[
f'(\beta) = \frac{1 - s^{-\frac{1}{p}}}{p} \ln (s) (\beta + r) - \frac{s^{-\frac{1}{p}}}{p} \beta^2
\]

∵ \( s > 1 \), we notice that \( f'(\beta) \) decreases as \( r \) increases, and:

\[
f'(\beta) = 0 \Leftrightarrow r = -\frac{\beta \ln (s) - \beta^2 s^{-\frac{1}{p}} + \beta}{\ln (s)} = g(\beta)
\]

Then we take the derivative of \( g(\beta), h(s), \) and \( i(s) \):

\[
g'(\beta) = \frac{\left(2 s^{-\frac{1}{p}} - 2\right) \beta - s^{-\frac{1}{p}} \ln (s) - \ln (s)}{\ln (s)} \geq h(s) \ln s
\]

\[
h'(s) = -\frac{s^{-\frac{1}{p}} \ln (s) - \beta s^{-\frac{1}{p}} + \beta}{\beta s} \geq -i(s) \beta s
\]

\[
i'(s) = \frac{s^{-\frac{1}{p}} \ln (s)}{\beta} \geq 0, \ s \geq 1
\]

∵ \( i'(s) \geq 0, i(s) \geq i(1) = 0, s \geq 1 \). That means \( h'(s) \leq 0, s \geq 1 \). So \( h(s) < h(1) = 0, s > 1 \). Hence, \( g'(\beta_0) < 0, s > 1 \). Now, assume \( f'(\beta_0) = 0 \) for \( \beta_0 \in [1, T] \). We know from Eq. (3) that
$r = g(\beta_0)$. For any $1 \leq \beta_1 < \beta_0$, we know $g(\beta_1) > g(\beta_0) = r$ according to $g'(\beta) < 0$. Because $f'(\beta)$ decreases when $r$ increases, we have:

$$f'(\beta_1) > \frac{1 - s^{-\frac{1}{p}}}{p} - \frac{\ln(s)(\beta_1 + g(\beta_1))}{ps^{-\frac{1}{p}}\beta_1^2} = 0$$

Likewise, for any $\beta < \beta_2 \leq T$, $f'(\beta_2) < 0$. These mean that if $f'(\beta)$ has a root $\beta_0$ in $[1, T]$, $f(\beta)$ is monotonically increasing in $[1, \beta_0]$, and monotonically decreasing in $[\beta_0, T]$. If $f'(\beta)$ does not have a root in $[1, T]$, then it is either monotonically increasing or monotonically decreasing in $[1, T]$ because $f'(\beta)$ is continuous in $[1, T]$. Therefore, in either case, the minimizer of $f(\beta)$ is either 1 or $T$.

Finally, we compare $f(1)$ and $f(T)$.

$$f(1) < f(T) \iff (r + 1)(1 - s^{-1}) < (r + T)(1 - s^{-1/T})$$
$$\iff (r + 1)(1 - (1 - p)^T) < (r + T)p$$
$$\iff r < \frac{pT + (1 - p)^T - 1}{1 - p - (1 - p)^T}$$

Theorem 1 states that the best constraint interval for Eq. (2) is either 1 or $T$. It also formulates the relationship between $r$, $p$, $T$, and $\beta$. By substituting $p = 0.5$ and $T = 16$, we get $\frac{pT + (1 - p)^T - 1}{1 - p - (1 - p)^T} = 14$. Figure 2b verifies the theoretical value: if cost ratios are less than 14, $\beta = 1$ costs the least. By using $p = 0.5$ and $r = 20$, we get $20 > \frac{0.5T + (0.5)^T - 1}{0.5 - (0.5)^T} \rightarrow 22 > T$. Figure 2a also verifies the theoretical value: curves ($T = 2, 4, 8, 16$) both favor $\beta = T$ to reach the smallest expected cost. The two figures confirm Theorem 1.

According to the analysis, we design the adaptive constraint evaluation interval as follows. Each trial receives its own constraint evaluation interval. In the beginning, we do not know the cost ratio $r$. The worst case is that the constraint evaluation is expensive. Using $\beta = 1$ as the initial value will lead to great cost. Thus, ACE selects $\beta = T$ as the initial value, which means the constraint evaluation occurs at the end of training. During the training of a trial, ACE records the primary cost and constraint cost on the fly. ACE computes the cost ratio using the average constraint cost divided by the average primary cost. After the cost ratio is computed, it picks the low-cost $\beta$ as the constraint evaluation interval by comparing $r$ and $\frac{pT + (1 - p)^T - 1}{1 - p - (1 - p)^T}$. Line 1 in Algorithm 1 implements the above statements.

3.4 Stratum truncation

We propose stratum truncation to use both optimization and constraint metrics to prune trials (Line 18 to 25 of Algorithm 1). It is motivated by several desiderata. First, we want to respect both the goal of optimization and constraint satisfaction in the early stopping. That requires pruning both the trials with bad optimization metric and the trials violating the constraints. Second, an invalid yet incomplete trial has a chance to meet the constraints with more training iterations. So it is not necessary to stop every invalid trial immediately. Third, as an HPO solution, it is preferred to avoid introducing additional hyperparameters such as penalty weights of the constraint metrics.

Our solution categorizes the trials into 3 groups and prunes the same fraction of low-rank trials in each group: (1) no-constraint: trials without constraint evaluation, (2) valid: trials meeting constraints, and (3) invalid: trials violating constraints. The no-constraint trials do not have constraint metrics evaluated at the current training iteration. The only performance indicator is the optimization metric. We rank the trials in this group by their optimization metric. For valid trials, we only care about their optimization metric, so we rank the trials in this group by their optimization metric. For the invalid group, we desire to penalize invalid trials by their violation amount ($g(x) - \tau$). The trials with larger violation amount should rank low. Thus, we sort the trials by their violation amount and use the optimization metric to break ties. Infeasible trials are not pruned immediately unless their violation amounts are on top. That gives the ‘close to valid’ trials a chance to meet the constraints later and potentially lead to better optimization results. At the same time, even if no infeasible trials are turned to feasible in the end, the promising trials in the valid group are kept running just like the case of unconstrained early stopping.
**Algorithm 1**: Adaptive Constraint-aware Early Stopping (ACE)

**Input**: hyperparameter configuration $x$; total training iterations $T$; constraint threshold $\tau$; running history $H$; truncation percentage $\mathcal{P}$.

1. Estimate the constraint evaluation interval $\beta$ based on Theorem 1
2. for $t \in [T]$ do
3. Train the model with $x$ for one iteration
4. Compute optimization metric $l(x, t)$ at the iteration $t$
5. if $t \mod \beta == 0$ and $l(x, t) \leq H.f^*$ then
6. Compute constraint metric $g(x, t)$ at the iteration $t$
7. if $g(x, t) \leq \tau$ then
8. trial_type = “valid”
9. $H.f^* = l(x, t)$
10. else
11. trial_type = ‘invalid”
12. end if
13. else
14. trial_type = “no_constraint”
15. end if
16. Update $H$
17. $H' = H$.subset(trial_type)
18. if trial_type == “invalid” then
19. $H'$.sort(keys=[violation_amount, optimization_metric])
20. else
21. $H'$.sort(keys=[optimization_metric])
22. end if
23. if $x$ is below $\mathcal{P}$% of $H'$ then
24. stop training
25. end if
26. end for

3.5 Reduce constraint evaluation overhead

While constraint evaluation helps prune ineligible trials, it adds significant overhead if the constraint metric is expensive to compute. To reduce such overhead, ACE performs constraint evaluation on promising trials only (Line 5 to 15 of Algorithm 1). Specifically, ACE maintains the global best feasible score, which is the best optimization metric value among the trials satisfying the constraint. Only if the current optimization metric is better than the global best feasible score does ACE compute the constraint of the current checkpoint. Otherwise, ACE skips the constraint evaluation for this checkpoint and marks the trial type of the current checkpoint as “no-constraint”. Note that bad trials in the “no-constraint” group still have the chance to be pruned due to our stratum truncation policy, even without constraint evaluation. With this low-overhead mechanism, ACE wastes less time in evaluating suboptimal trials.

4 Experimental evaluation

We evaluate our algorithm under a fairness constraint and a robustness constraint respectively. Since ACE is an early stopping approach, our baselines are no-stopping and a state-of-the-art early stopping method, ASHA (Li et al., 2020). ASHA is a parallel early stopping method using successive halving (Jamieson and Talwalkar, 2016) to allocate budgets for trials. ACE uses 25% as the truncation percentage for all the experiments. We analyze the impact of the truncation percentage in Appendix B. The reported results are the average of three random seeds in all the experiments.

4.1 Fairness constraint

We follow Fairlearn (Bird et al., 2020) to preprocess the UCI credit card default dataset (Yeh and Lien, 2009). The processed dataset has 30k clients with 22 features, which we split 70/30% for training/validation. The fairness constraint is Equalized-Odd-Difference (EOD) (Bird et al., 2020) =
max(|FPR1 − FPR2|, |FNR1 − FNR2|), where FPR and FNR mean false positive rate and false negative rate, respectively. EOD quantifies the accuracy disparity experienced by different groups. We search hyperparameters of LightGBMs under two threshold levels: (i) the hard constraint: EOD ≤ 0.25 and (ii) the easy constraint: EOD ≤ 0.325. For each case, we evaluate ACE’s performance with unconstrained random search (Bergstra and Bengio, 2012) or constrained blend search (Wang et al., 2021a). Blend search combines global and local search and prioritizes their suggestion on the fly. Its implementation in the FLAML library (Wang et al., 2021b) can handle constrained optimization. It penalizes the optimization metric with the amount of constraint violation. Since the constrained HPO needs constraint information, we implement the constraint callbacks for the baselines. The callbacks compute constraint metrics for a searcher. The search budget is one hour. The optimization metric is Area Under the Curve (AUC) of ROC (Davis and Goadrich, 2006). Appendix C summarizes the rest of experiment setup.

Table 1 shows the results under the fairness constraint. “Time to best” means the time to find the best feasible trial within each run from the beginning of search. For baselines without the constraint callback, after the tuning, we sort the searched trials by their optimization metric and compute constraints from top to down until we find the first feasible trial. So their "time to best" is longer than the one hour budget. If a method can find the highest feasible AUC compared to other methods, then smaller "Time to best" is better. Otherwise, smaller “Time to best” just indicates a method converges to a suboptimal point early.

ACE outperforms the baselines in terms of feasible AUC when using both searchers under both easy and hard constraints. In blend search with the hard constraint (top Table 1), ACE needs only 1/2 of the search budget to attain the best feasible AUC. ASHA and no-stopping converge to worse feasible AUC even when using the full budget. Their feasible AUC are not improved after 5 minutes. Without considering constraint results, ASHA wastes time in training infeasible trials. Furthermore, although random search is an unconstrained searcher, ACE improves feasible AUC by 1.1% in the hard constraint and makes it perform as well as the constrained searcher. We make a case study of two trials both appearing in ACE and ASHA, shown in Figure 1. ASHA wrongly prunes a promising trial (blue curve) very quickly and spends unnecessary training time on an infeasible trial (red curve). ACE successfully prunes them at the appropriate iteration. It highlights that adding the constraint violation in the performance ranking makes ACE allocate the training budget to promising trials. For the easy constraint, constraint violations are rare. Our constrained early stopping gets close to constraint-agnostic early stopping, as few trials are categorized into the “invalid” group. In this case, ACE still performs as well as ASHA (bottom Table 1). It implies our stopping policy can also work well with limited utility of constraint feedback.

4.2 Robustness constraint

We use DistilBERT (Sanh et al., 2019) to predict the sentiment of a given sentence from the Stanford Sentiment Treebank (SST2) of GLUE (Wang et al., 2018). DistilBERT is a small and fast transformer model, which uses BERT as a teacher and is pretrained on the

| Constraint | Searcher | Early stopping policy | Total trials | Best feasible AUC (%) | Time to best |
|------------|----------|-----------------------|--------------|-----------------------|-------------|
| EOD ≤ 0.25 (hard) | Blend search | No-stopping | 276.0 | 84.95 ± 0.43 | 0h 5m 5s |
| | | No-stopping w/ constraint callback | 626.3 | 84.98 ± 0.51 | 1h 1m 7s |
| | | ASHA | 3,664.3 | 82.88 ± 3.13 | 1h 2m 45s |
| | | ASHA w/ constraint callback | 4,252.0 | 85.06 ± 0.35 | 0h 5m 19s |
| | | ACE | 1,799.3 | **85.53 ± 0.03** | 0h 29m 09s |
| | Random search | No-stopping | 37.0 | 82.28 ± 0.45 | 1h 0m 15s |
| | | ASHA | 3,497.7 | 84.19 ± 0.35 | 1h 0m 53s |
| | | ACE | 283.7 | **85.38 ± 0.06** | 0h 39m 09s |
| EOD ≤ 0.325 (easy) | Blend search | No-stopping | 694.3 | 85.85 ± 0.03 | 0h 4m 0s |
| | | No-stopping w/ constraint callback | 307.0 | 85.83 ± 0.05 | 0h 15m 57s |
| | | ASHA | 3,763.3 | 85.82 ± 0.08 | 0h 1m 15s |
| | | ASHA w/ constraint callback | 3,677.3 | 85.81 ± 0.11 | 0h 24m 15s |
| | | ACE | 2,197.7 | **85.89 ± 0.00** | 0h 54m 22s |
| | Random search | No-stopping | 37.0 | 85.71 ± 0.10 | 1h 0m 03s |
| | | ASHA | 3,596.7 | 85.77 ± 0.03 | 1h 0m 17s |
| | | ACE | 1,200.0 | **85.79 ± 0.07** | 0h 19m 37s |

Table 1: Best feasible AUC under the fairness constraint.
same corpus as BERT in a self-supervised fashion. SST is split into 67,349 and 872 sentences for training and validation respectively, where the sentences are encoded by the DistilBERT's pretrained tokenizer. The robustness constraints come from the NLP model CHECKLIST (Ribeiro et al., 2020), which provides a sentiment test suite to check the prediction invariance in the presence of certain perturbation or certain corner cases. CHECKLIST measures the test score by the failure rate, a portion of predictions failing to remain original answers with perturbation. We use 21 test tasks in the test suite, where each task has 300 test cases. Average failure rate (AFR) is chosen to aggregate the results of the 21 test tasks. We use random search to find the hyperparameters for finetuning DistilBERT under four threshold levels: AFR $\leq 0.19$, AFR $\leq 0.20$, AFR $\leq 0.24$, and AFR $\leq 0.25$. We report average accuracy of three random seeds for each threshold. The rest of experiment setup are summarized in Appendix D.

![Figure 3](image)

Figure 3: Best feasible accuracy under the robustness constraint. The column name represents different robustness constraint thresholds, where AFR is the short name of average failure rate. The values in the table are the best feasible accuracy ($\%$). Successful rate indicates how many times an early stopping policy can find at least one feasible trial among three random seeds. The figure displays that ACE is robust to find feasible trials and outperforms baselines in most constraints.

Figure 3 exhibits that ACE achieves 100% successful rate to get feasible trials under all the robustness constraints, while no-stopping and ASHA only attain 100% successful rate under AFR $\leq 0.25$. For the best feasible accuracy (the table in Figure 3), ACE obviously outperforms state-of-the-art ASHA under all the robustness constraints. With the consideration of constraint values, ACE can wisely invest time on feasible trials. ACE also beats no-stopping under the first three constraint thresholds and performs competitively under AFR $\leq 0.25$. The best feasible trials of no-stopping under AFR $\leq 0.25$ possesses the worst accuracy in the initial training iterations. Hence, ACE prunes these two trials accordingly, as well as ASHA does. The results reveal that reducing training overhead on inferior trials sometimes leads to wrongful termination of promising candidates. Addressing this limitation would be promising future work.

### 4.3 Ablation study

We analyze ACE design choices by evaluating (i) different stopping criterion and (ii) static/adaptive constraint evaluation intervals in Table 2 and Table 3 respectively. Since random search generates the identical sequences of hyperparameters given the same random seed, we select it to compare different choices fairly for the ablation study.

| Constraint | Method | Stopping criterion | Low-overhead evaluation | Best feasible AUC ($\%$) |
|------------|--------|---------------------|--------------------------|--------------------------|
| EOD $\leq 0.25$ (hard) | ACE$_{hard}$ | hard stopping | ✓ | 84.94 ± 0.31 |
| | ACE$_{noskip}$ | stratum | | 85.37 ± 0.02 |
| | ACE | stratum | ✓ | 85.38 ± 0.06 |
| EOD $\leq 0.325$ (easy) | ACE$_{hard}$ | hard stopping | ✓ | 85.74 ± 0.05 |
| | ACE$_{noskip}$ | stratum | | 85.69 ± 0.03 |
| | ACE | stratum | ✓ | 85.79 ± 0.07 |

Our stratum truncation in ACE is a soft stopping approach, which tolerates invalid checkpoints. A hard stopping policy terminates a trial immediately as soon as the trial encounters the first invalid
We study the problem of effective early stopping for constrained HPO, which saves cost in training.

ACE’s stratum truncation policy is designed for a single constraint metric. Although in practice, one ACE can be quickly adopted into different scenarios as the benefit of RAY ecosystem. As a limitation, ACE’s adaptive constraint interval is merely derived from the constraint cost consideration. It is an interesting question for future work whether it is beneficial to adjust the constraint evaluation interval according to the feasibility consideration. Table 2 shows that ACE_{hard} decreases performance for both easy and hard fairness constraints. The constraint values do not increase or decrease monotonically. It might temporarily violate the constraint and meet the constraint late, such as the blue curve in Figure 1. Just considering constraint validity, ACE_{hard} might terminate trials at wrong iterations. Furthermore, ACE_{noskip} faithfully evaluates constraints without skipping suboptimal trials which have inferior optimization metrics compared to the best feasible trial. Table 2 indicates that the reduction of constraint evaluation overhead improves ACE performance for the easy constraint and does not degrade the performance for the hard constraint. ACE_{noskip} suffers from unnecessary constraint cost on suboptimal trials, especially when the constraint is expensive to evaluate.

Next, we study how constraint intervals affect the performance by replacing ACE’s adaptive constraint interval with static values. ACE_{β=T} enforces all the trials to check constraints once at the end of the training iteration. A trial’s constraint metric is computed for its best checkpoint (with the best optimization metric). ACE_{β=1} fixes β = 1 for all the trials. Table 3 demonstrates that ACE can adjust the constraint interval for different constraint characteristics. For the cheap constraint (low cost ratio), ACE assigns 87% of trials β = 1. For the expensive constraint (high cost ratio), ACE assigns 64% of trials β = T. The results match the theoretical prediction in Theorem 1. Since Eq. (2) also enforces all the trials to check constraints once at the end of T, β is not fixed for all the trials. It is not surprising that ACE_{β=1} can achieve competitive performance of ACE for the cheap constraint but weaker for the expensive constraint, as our theory predicts. ACE_{β=T} has a chance in theory to outperform ACE for the expensive constraint, since ACE_{β=T} largely reduces the constraint evaluation overhead. ACE_{β=T} indeed searches 1.8 times more trials than ACE and 3.9 times more than ACE_{β=1}. Nevertheless, a trial’s best checkpoint is not equal to its best feasible checkpoint. Some feasible trials in ACE are considered as infeasible by ACE_{β=T} for that reason. Thus, ACE_{β=T} ends up performing poorly. ACE selects β = 1 for trials with large T (See Figure 2a). Even though ACE selects β = T for a trial with small T, its small number of checkpoints reduces the chance for ACE to use wrong checkpoint. ACE’s adaptive constraint interval is merely derived from the constraint cost consideration. It is an interesting question for future work whether it is beneficial to adjust the constraint evaluation interval according to the feasibility consideration.

### Table 3: Ablation study for the adaptive constraint evaluation interval.

| Constraint | Cost ratio | Method    | β = 1 (%) | β = T (%) | Best feasible score (%) |
|------------|------------|-----------|-----------|-----------|------------------------|
| EOD ≤ 0.25 (cheap) | 1.94       | ACE_{β=1} | 100       | 0         | 85.38 ± 0.05           |
|             |            | ACE_{β=T} | 0         | 100       | 84.61 ± 0.57           |
|             |            | ACE       | 87        | 13        | 85.38 ± 0.06           |
| AFR ≤ 0.2 (expensive) | 23.98     | ACE_{β=1} | 100       | 0         | 84.33 ± 1.80           |
|             |            | ACE_{β=T} | 0         | 100       | 79.82 ± 2.93           |
|             |            | ACE       | 56        | 64        | 85.93 ± 1.15           |

5 Conclusion

We study the problem of effective early stopping for constrained HPO, which saves cost in training infeasible trials and explores other promising and feasible candidates. For broader impact, ACE calls for attention to practical HPO scenarios where application constraints must be met for model deployment. It highlights the computational challenge of constrained HPO and opportunities for cost saving through a new approach of early stopping. It also reveals important characteristics of constraints to consider in designing a generic approach, such as the difficulty to meet and the computation cost to evaluate. It provides a new point of research view toward constrained HPO. ACE is extensible to diverse search algorithms and shallow and deep ML models. It is implemented on top of RAY, a hyperparameter tuning framework, which supports 14 search techniques and integrates a variety of ML frameworks, including PyTorch, Tensorflow, HuggingFace, LightGBM, etc. Thus, ACE can be quickly adopted into different scenarios as the benefit of RAY ecosystem. As a limitation, ACE’s stratum truncation policy is designed for a single constraint metric. Although in practice one could combine multiple constraint metrics into one, some information can be lost in the combination. More advanced extensions for multiple constraints might make ACE flexible to prioritize multiple constraints in complicated scenarios.
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A Derivation of Equation (2)

The first part of Eq. (1) is simplified as:

\[(1 - p)^z[C_1 z + C_2 z T] = (1 - p)^z[rC_2 z + C_2 z \beta] = (1 - p)^z C_2 (r + \beta) z.\]

The second part of Eq. (1) can be simplified as:

\[\sum_{k=1}^{z} (1 - p)^{k-1} p[C_1 k + C_2 k \beta] = \sum_{k=1}^{z} (1 - p)^{k-1} p[rC_2 k + C_2 k \beta]\]

\[= p C_2 (r + \beta) \sum_{k=1}^{z} k (1 - p)^{k-1}\]

\[= p C_2 (r + \beta) \frac{\sum_{k=1}^{z} k (1 - p)^{k-1}}{p}\]

\[= p C_2 (r + \beta) \frac{\sum_{k=0}^{z} k (1 - p)^{k-1}}{p}\]

\[= p C_2 (r + \beta) \frac{(z + 1)(1 - p)z - (1 - p)^{z+1}}{p^2}\]

\[= p C_2 (r + \beta) \frac{1 - (1 - p)^{z}(zp + 1)}{p^2}\]

Combining the above equations, we get Eq. (2).

\[E[C] = (1 - p)^z C_2 (r + \beta) z + p C_2 (r + \beta) \frac{1 - (1 - p)^{z}(zp + 1)}{p^2}\]

\[= C_2 (r + \beta) \frac{zp(1 - p)^z + 1 - (1 - p)^{z}(zp + 1)}{p}\]

\[= C_2 (r + \beta) \frac{1 - (1 - p)^z}{z}.\]

Figure 4: Truncation percentage analysis of ACE’s stratum truncation. The label under each point represents AUC (%) and the number of total trials. The best feasible AUC is fairly stable as the truncation percentage varies from 3% to 25%.

B Truncation percentage analysis

ACE’s stratum truncation terminates a fraction of low-rank trials according to the “truncation percentage” (See Section 3.4). We analyze the impact of the percentage by searching hyperparameters
of LightGBM under the fairness constraints (See Section 4.1). Since random search can generate the same sequences of hyperparameters in different “truncation percentage”, we use it to report the feasible AUCs with three random seeds (20, 21, and 22). Figure 4 exhibits that 13% as truncation percentage leads ACE to perform the best for both hard ($EOD \leq 0.25$) and easy ($EOD \leq 0.325$) constraints. 50% as truncation percentage is the most nature choice, but 50% decreases the feasible AUC for the easy constraint. The number of total trials increases from 3% to 75%. The large truncation percentages stop more trials than small truncation percentages. We also observe that when truncation percentage varies from 3% to 25%, the best feasible AUC is fairly stable. These observations suggest that it is reasonable to use 25% as the default truncation percentage for the stratum truncation and the performance of ACE is not particularly sensitive to this choice.

C  Fairness experiment setup

The fairness experiments of Section 4.1 are run on 12 cores of Intel i7-6850K@3.6 GHz. We search hyperparameters of LightGBM under a fairness constraint, where its search space follows FLAML (Wang et al., 2021b), shown in Table 4. The types in the table follow RAY (Moritz et al., 2018). ASHA follows the default values of RAY library (Moritz et al., 2018): reduction factor = 4, brackets = 1, grace period = 1, and max time units = 21,000 (the number of training data). The random seeds of the experiments are 20, 21, 22. The max concurrent trials are 4. The fairness experiments of in Section 4.3 also follows the same setup here.

| Name            | Type               | Lower value | Upper value | Initial value |
|-----------------|--------------------|-------------|-------------|---------------|
| n_estimators    | ray.tune.lograndint | 4           | the number of instances | 4             |
| num_leaves      | ray.tune.lograndint | 4           | the number of instances | 4             |
| min_child_samples | ray.tune.lograndint | 2           | 129         | 20            |
| learning_rate   | ray.tune.loguniform | 1/1024  | 1.0         | 0.1           |
| log_max_bin     | ray.tune.lograndint | 3           | 11          | 8             |
| colsample_bytree | ray.tune.uniform   | 0.01        | 1.0         | 1.0           |
| reg_alpha       | ray.tune.loguniform | 1/1024  | 1024        | 1/1024        |
| reg_lambda      | ray.tune.loguniform | 1/1024  | 1024        | 1.0           |

D  Robustness experiment setup

The robustness experiments of Section 4.2 are run on 64 cores of AMD EPYC 7282 and 8 NVIDIA RTX A5000. PYTHON 3.6 environment includes FLAML 0.6.9, RAY 1.10, CHECKLIST 0.0.11, and HUGGINGFACE-HUB 0.4.0. We search hyperparameters for finetuning DistilBERT on SST2 under a robustness constraint. The search space is motivated by FLAML library (Wang et al., 2021b), as shown in Table 5. The types in the table follow RAY (Moritz et al., 2018). ASHA follows the default values of RAY library (Moritz et al., 2018): reduction factor = 4, brackets = 1, grace period = 1, and max time units = 67,349 (the number of training data). The random seeds of the experiments are 19, 20, 21. Th max concurrency trials are 4. The search budget is three hours. The robustness experiments of in Section 4.3 also follows the same setup here.

E  Comparison between geometric and linear interval

Given the reduction factor = 4, ASHA examines trial performance by geometric intervals, i.e., 1, 4, 16, 64, .... In contrast, ACE check trials by linear intervals, i.e., 1, 2, 3, .... The different interval motivates us to study the performance of geometric intervals in constrained early stopping. We extend ASHA with adaptive constraint interval and stratum truncation. If the adaptive constraint interval suggests $\beta = 1$, we enforce ASHA to compute constraint values by geometric intervals. If the adaptive constraint interval suggests $\beta = T$, ASHA uses a trial’s best checkpoint to evaluate constraint values at the last training iteration. Notice that Theorem 1 is developed by the linear interval assumption. We merely borrow it to suggest constraint intervals, rather than develop a
Table 5: The hyperparameter space of finetuning DistilBERT

| Name                     | Type                | Lower value | Upper value | Initial value |
|--------------------------|---------------------|-------------|-------------|---------------|
| learning_rate            | ray.tune.loguniform| 1e-6        | 1e-3        | 1e-5          |
| num_train_epochs         | ray.tune.loguniform| 0.1         | 10.0        | 3.0           |
| per_device_train_batch_size | ray.tune.choice    | 4, 8, 16, 32| 32          |               |
| warmup_ratio             | ray.tune.uniform   | 0.0         | 0.3         | 0.0           |
| weight_decay             | ray.tune.uniform   | 0.0         | 0.3         | 0.0           |
| adam_epsilon             | ray.tune.loguniform| 1e-8        | 1e-6        | 1e-6          |
| seed                     | ray.tune.choice    | 40, 41, 42, 44| 42        |               |

New theorem. We use blend and random search to search hyperparameters of LightGBM under the hard fairness constraint (EOD \(\leq 0.25\)). In Table 6, we observe the stratum truncation and adaptive constraint interval can improve constraint-agnostic ASHA. Since the constrained ASHAs do not have the low-overhead constraint evaluation, we report ACE\(_\text{noskip}\) to compare their performance. ACE\(_\text{noskip}\) outperforms ASHA\(_\text{stratum}\) and ASHA\(_\text{stratum, not fixed}\). A trial’s best checkpoint is not equal to its best feasible checkpoint. The large interval space of ASHA makes it unlikely to locate feasible trials at correct checkpoints. Thus, using linear intervals performs better than using geometric intervals.

Table 6: Geometric vs. linear interval

| Searcher    | Method       | Interval type | Stopping criterion | Constraint interval | Best feasible AUC (%) |
|-------------|--------------|---------------|--------------------|---------------------|-----------------------|
| Blend search| ASHA         | geometric     | no-stratum         | fixed               | 85.05 ± 0.35          |
|             | ASHA\(_\text{stratum}\) | geometric | stratum            | fixed               | 85.35 ± 0.07          |
|             | ASHA\(_\text{stratum, not fixed}\) | geometric | stratum            | not-fixed           | 85.16 ± 0.07          |
|             | ACE\(_\text{noskip}\)     | linear       | stratum            | not-fixed           | **85.41 ± 0.09**      |
| Random search| ASHA         | geometric     | no-stratum         | fixed               | 84.19 ± 0.35          |
|             | ASHA\(_\text{stratum}\) | geometric | stratum            | fixed               | 85.27 ± 0.16          |
|             | ASHA\(_\text{stratum, not fixed}\) | geometric | stratum            | not-fixed           | 85.32 ± 0.17          |
|             | ACE\(_\text{noskip}\)     | linear       | stratum            | not-fixed           | **85.37 ± 0.02**      |
Table 7: twenty-one test tasks and examples

| #  | Test task name                           | Example                                                                 |
|----|-----------------------------------------|-------------------------------------------------------------------------|
| 1  | Single positive words                   | fun                                                                     |
| 2  | Single negative words                   | boring                                                                  |
| 3  | Single neutral words                    | saw                                                                     |
| 4  | Sentiment-laden words in context        | That staff is boring.                                                  |
| 5  | Neutral words in context                | I see this aircraft.                                                   |
| 6  | Intensifiers                            | This is an incredibly unpleasant service.                              |
| 7  | Change neutral words with BERT          | @USAirways my in-laws just Cancelled Flighted 4 tonight. U auto rebooked 4 just on Tuesday that doesn’t work. Can you help reFlight Booking Problems them? |
| 8  | Add positive phrases                    | @JetBlue so technically I could drive to JFK now and put in. Request for tomorrow’s flight. You are sweet. |
| 9  | Add negative phrases                    | @JetBlue we are well aware. Insufficient info. No options. You are poor. |
| 10 | Add random urls and handles             | @united My flying United is over...sorry. The Captain still had 20 minutes of pre-flight preparations to make while we sat with no air! https://t.co/befys3 |
| 11 | Punctuation                             | @united pleasantly surprised with quality of service and flight. Flew LGA-CLE-DEN, Friendly crew. Love the concept of #byod #worksnicely. |
| 12 | Typos                                   | @VirginAmerica - can you tweet me the Cancelled Flight/chng fee for a flight? or can I rebook under one of your affiliates? If so, who are affiliates? |
| 13 | 2 typos                                 | @united @anricular 0162431184663.uu3 o fyour agents said we would be refunded. Agents said United should never have sold us the ticket. |
| 14 | Contractions                            | @united didn’t get her name. She was not in our group. She was sitting behind us. Think it was window seat #40? We only overheard... |
| 15 | Change names                            | @AmericanAir You guys did an amazing job today! Know it’s hard; thanks to Kate Appleton for all her hard work reFlight Booking Problems my friends and me! |
| 16 | Change locations                        | @SouthwestAir Gate attendant at McCarran C16 (Vegas to Dallas) went above and beyond. After a long day of frustration it was welcome. |
| 17 | Change numbers                          | @SouthwestAir Your onboard wifi is so bad it’s taking me 20 minutes to send this tweet. Working is off the table. #disappointed |
| 18 | Protected race                          | Melanie is a black migrant.                                           |
| 19 | Protected sexual                        | Jesse is an asexual father.                                           |
| 20 | Protected religion                      | Ryan is a Christian student.                                          |
| 21 | Protected nationality                   | Destiny is a Chinese developer.                                       |