Swelling, structure, and phase stability of compressible microgels

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Microgels are soft colloidal particles that, when dispersed in a solvent, swell and deswell in response to changes in environmental conditions, such as temperature, concentration, and pH. Using Monte Carlo simulation, we model bulk suspensions of microgels that interact via Hertz elastic interparticle forces and can expand or contract via trial moves that allow particles to change size in accordance with the Flory-Rehner free energy of cross-linked polymer gels. We monitor the influence of particle compressibility, size fluctuations, and concentration on bulk structural and thermal properties by computing particle swelling ratios, radial distribution functions, static structure factors, osmotic pressures, and freezing densities. For microgels in the nanoscale size range, particle compressibility and associated size fluctuations suppress crystallization, shifting the freezing transition to a higher density than for the hard-sphere fluid. As densities increase beyond close packing, microgels progressively deswell, while their intrinsic size distribution grows increasingly polydisperse.

1 Introduction

Microgels are soft, compressible colloidal particles, typically composed of cross-linked polymer networks that, when dispersed in a solvent, can swell significantly in size and can respond sensitively to environmental changes. Equilibrium particle sizes are determined both by the elasticity of the gel network and by temperature, particle concentration, and solvent quality. Ionic microgels, which acquire charge via dissociation of counterions, further respond to changes in pH and salt concentration. Tunable particle size results in unusual materials properties, with practical applications to filtration, rheology, and drug delivery.

Over the past two decades, numerous experimental and modeling studies have characterized the elastic properties of single microgel particles and the equilibrium and dynamical behavior of bulk suspensions. Connections between single-particle properties, such as swelling ratio, and bulk properties, such as osmotic pressure, thermodynamic phase behavior, pair structure, and viscosity, have been probed experimentally by static and dynamic light scattering, small-angle neutron scattering, confocal microscopy, and osmometry. While the swelling/deswelling behavior of microgels has been extensively studied, the full implications of elasticity and compressibility of these soft colloids for bulk suspension properties remain only partially understood.

Previous modeling studies have examined the influence of elastic interparticle interactions on structure and phase behavior.

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In an extensive simulation survey, Pamiès et al. mapped out the thermodynamic phase diagram of a model of elastic, but incompressible, spheres interacting via a Hertz pair potential. For a related model of ionic microgels, one of us and coworkers recently applied molecular dynamics simulation and thermodynamic perturbation theory to compute the osmotic pressure and static structure factor of a suspension of Hertzian spheres that interact also electrostatically, via an effective Yukawa pair potential. At the single-particle level, numerous studies have established that the classic Flory-Rehner theory of swelling of cross-linked polymer networks, though originally developed for macroscopic gels, provides a reasonable description also of the elastic properties of microgel particles. However, the implications of particle compressibility and intrinsic size polydispersity for bulk properties of microgel suspensions have not been fully explored. The purpose of this paper is to analyze the combined influences of particle elasticity, compressibility, and associated size fluctuations on bulk thermal and structural properties of microgel suspensions.

The remainder of the paper is organized as follows. In Section 2, we describe a model of microgels as compressible spheres, whose swelling is governed by a single-particle free energy derived from the Flory-Rehner theory of cross-linked polymer networks, and whose interparticle interactions are represented by a Hertz elastic pair potential. In Section 3, we outline Monte Carlo simulation methods by which we modeled bulk suspensions of compressible, size-fluctuating microgels. Section 4 presents numerical results for thermodynamic properties, specifically osmotic pressure and liquid-solid phase behavior, and structural properties, including particle volume fraction.
radial distribution function, and static structure factor. Finally, in Section 5, we summarize and conclude.

2 Model

2.1 Swelling of microgel particles

We model a microgel as a spherical particle of dry (collapsed, unswollen) radius $a_0$ and swollen radius $a_s$, consisting of a cross-linked network of $N_m$ monomers, with a uniform distribution of cross-linkers that divide the network into $N_{ch}$ distinct chains (see Fig. 1). Although idealized, this simple model provides a reference that can be generalized to heterogeneous microgels with nonuniform distribution of cross-linkers, such as core–shell\textsuperscript{7–19,41,52,53} or hollow\textsuperscript{54–56} microgels. To highlight the results from stretching of polymer coils, subject to the constraints stemming from structural changes in surrounding solvent upon stretching a polymer coil, while the Gaussian coil approximation is valid only for swelling ratios not exceeding the polymer contour length.\textsuperscript{56} Given the Flory–Rehner free energy [eqn (1)], the size of a single, isolated microgel (i.e., in a dilute solution) fluctuates according to a probability distribution,

$$P_q(a) \propto \exp[-\beta F(a)].$$

In thermal equilibrium, an isolated, swollen microgel in a dilute solution has a most probable radius $a_m$, corresponding to the maximum of this distribution (i.e., minimum free energy). A suspension of particles thus has a fluctuating particle size distribution, i.e., dynamical size polydispersity, governed by eqn (2).

2.2 Microgel pair interactions

While swelling of isolated microgels in dilute solutions is governed only by intraparticle interactions, modeled by eqn (1), swelling in concentrated solutions is influenced also by interparticle interactions. To account for this additional influence, we model the repulsion between a pair of microgel particles, of instantaneous radii $a_i$ and $a_j$ at center-to-center separation $r$, \textit{via} a Hertz effective pair potential,\textsuperscript{47}

$$\eta(r) = \begin{cases} 
\varepsilon \left(1 - \frac{r}{a_i + a_j}\right)^{5/2}, & r < a_i + a_j \\
0, & r \geq a_i + a_j.
\end{cases}$$

The total internal energy associated with pair interactions is then given by

$$U = \sum_{i<j} \eta(r_{ij}),$$

where $r_{ij}$ is the distance between the centers of particles $i$ and $j$. For particles of average volume $v = (4\pi/3)a^3$, with angular brackets denoting an ensemble average over configurations, the Hertz pair potential amplitude is

$$\varepsilon = \frac{4Yv}{5\pi(1-\nu^2)},$$

which depends on the elastic properties of the gel through Young's modulus $Y$ and the Poisson ratio $\nu$.\textsuperscript{17} Scaling theory of polymer gels in good solvents\textsuperscript{58} predicts that the bulk modulus scales linearly with temperature and density of cross-linkers (or chain number): $Y \sim T N_{ch}/v$. The denser the cross-links, the stiffer the gel. It follows that the reduced amplitude, $e^* = \varepsilon/a_0$, is essentially independent of temperature and particle volume, neglecting dependence of $\nu$ on $a_0$ and scales linearly with $N_{ch}$.

The elastic properties of bulk, water-swollen hydrogels have been measured using scanning force microscopy.\textsuperscript{59} For poly(N-isopropylacrylamide) (PNIPAM) hydrogel with 0.25 mol% cross-linker,
Young’s modulus was determined as 0.33 kPa in the fully swollen state at 10 °C and 13.9 kPa in the collapsed state at 40 °C. In contrast, poly(acrylamide) (PA) hydrogels with cross-linker between 1 and 5 mol% have Young’s moduli measured in the range from 90 to 465 kPa at 20 °C. Typical Poisson ratios for these gels are \( \nu \approx 0.5 \). In Section 4, we appeal to such measurements to select realistic pair potential parameters for our simulations.

### 2.3 Suspensions of swollen microgels

At constant \( T \), the equilibrium thermodynamic state of a suspension of \( N \) particles in a volume \( V \) depends on the average number density, \( n = N/V \). For a suspension of microgels, the dry volume fraction, \( \phi_0 = (4\pi/3)na_0^3 \), is defined as the ratio of the fraction of the total volume occupied by the particles in their dry state. Correspondingly, the swollen volume fraction is defined as the ratio of the most probable volume of a swollen particle to the volume per particle: \( \phi = (4\pi/3)n(a^3) = \phi_0(\xi^3) \). In suspensions of highly swollen particles, \( \phi \) can substantially exceed \( \phi_0 \). For reference, we also define the generalized volume fraction \( \xi = (4\pi/3)na_s^3 = \phi_0(\xi_s^3) \). Note that \( \xi \geq \phi \) (since \( a_s \geq a \)) and that \( \phi \) and \( \xi \) have no upper bounds. In particular, in concentrated suspensions beyond close packing, it is possible that \( \xi > 1 \) and \( \phi > 1 \). At such high concentrations, crowded microgel particles may not only compress in size, but may also distort in shape. The presently studied model allows the former, but not the latter, response to crowding, although the Hertz potential may be interpreted as allowing for faceted deformations. In a more refined model, the microgels could be represented as elastic spheres or ellipsoids that can compress along three axes with an associated deformation energy.

### 3 Computational methods

To study the influence of particle compressibility and fluctuating size polydispersity on thermal and structural properties of bulk microgel suspensions, we performed a series of constant-NVT Monte Carlo (MC) simulations of systems of particles modeled by the Flory-Rehner size distribution [eqn (2)] and the Hertz pair potential [eqn (3)], as described in Section 2. For \( N \) particles in a cubic box of fixed volume \( V \) with periodic boundary conditions at fixed temperature \( T \), we made trial moves consisting of combined particle displacements and size changes. Following the standard Metropolis algorithm, a trial displacement and change in swelling ratio, from \( x \) to \( x' \), was accepted with probability

\[
P_{\text{acc}} = \min\{ \exp[-\beta(\Delta U + \Delta F)], 1 \},
\]

where \( \Delta U \) is the change in internal energy [eqn (4)] associated with interparticle interactions and \( \Delta F = F(x') - F(x) \) is the change in free energy [eqn (1)] associated with swelling. At equilibrium, the particles adopt a size distribution \( P(x;\phi_0) \) that depends on the dry particle volume fraction \( \phi_0 \) and minimizes the total free energy of the system. Since the particles modeled here are compressible and polydisperse, the generalized volume fraction can exceed close packing of monodisperse hard spheres (\( \phi \approx 0.74 \)). Such high concentrations create a strong interplay between the Hertz elastic energy and the Flory-Rehner swelling free energy.

To guide analysis of phase behavior, we computed structural properties that probe interparticle pair correlations and thermodynamic properties that govern phase stability. First, we determined the radial distribution function \( g(r) \) by standard means, histogramming into radial bins the radial separation \( r \) of particle pairs in each configuration and averaging over configurations. Second, we computed the static structure factor \( S(q) \), proportional to the Fourier transform of \( g(r) \) and to the intensity of scattered radiation at scattered wave vector magnitude \( q \).

For a system of \( N \) particles, the orientationally averaged two-particle static structure factor is defined as

\[
S(q) = \frac{2}{N} \sum_{i<j=1}^{N} \left\langle \frac{\sin(qr_{ij})}{qr_{ij}} \right\rangle + 1,
\]

where angular brackets again denote an ensemble average over particle configurations – the same configurations as used to compute \( g(r) \). Finally, we computed the osmotic pressure of the system from the virial theorem

\[
\beta \pi/n = 1 + \frac{3}{Nk_B T} \sum_{i<j=1}^{N} \langle r_{ij} f(r_{ij}) \rangle,
\]

where \( f(r) = -v_H(r) \) is the Hertz pair force.

### 4 Results and discussion

From simulations of \( N = 500 \) particles initialized on an fcc lattice, we analyzed the equilibrium particle swelling ratio, structural properties, and osmotic pressure over a wide range of densities. The results presented below represent statistical averages of particle coordinates and radii over 1000 independent configurations, separated by intervals of 100 MC steps (total of \( 10^5 \) steps), following an initial equilibration phase of \( 5 \times 10^4 \) MC steps, where a single MC step is defined as one combined trial displacement and size change of every particle. To confirm that the system had equilibrated, we computed the total internal energy and pressure and checked that both quantities had reached stable plateaus. A typical snapshot of the system is shown in Fig. 2.

In the low-density (dilute) regime, the initial lattice structure rapidly fell apart, as particles freely diffused through the system, implying a stable fluid phase. In the high-density (concentrated) regime, strongly interacting particles remained in the fcc lattice structure, consistent with a stable or metastable crystalline phase. At intermediate densities, relative stability of fluid and solid phases depended on the interparticle interactions. We emphasize that we did not attempt to determine thermodynamic phase stability, which would require more extensive simulations and thermodynamic integration to compute total free energies and perform coexistence analyses. Nor did we
investigate the glass transition, for which purpose molecular dynamics simulation would be better suited. Nevertheless, our results suggest that compressibility of microgels may significantly alter the phase diagram of strictly Hertzian spheres.

To explore dependence of bulk properties on particle size and pair interactions, we studied two systems distinguished by widely different particle sizes and interactions. The first system is a suspension of relatively small microgels (nanogels) of dry radius \( a_0 = 10 \text{ nm} \), comprising \( N_m = 2 \times 10^9 \) monomers – consistent with monomers of radius 0.3 nm – and \( N_{\text{ch}} = 200 \) chains, corresponding to 0.05 mol% of cross-linker (assuming two chains per cross-linker). A typical snapshot from an MC simulation of a suspension of compressible, spherical microgel particles in a cubic box with periodic boundary conditions is shown in Fig. 2. The particles interact via a Hertz pair potential with reduced amplitude \( \varepsilon^* = 1.5 \times 10^3 \). With increasing concentration \( \zeta \), as close packing is approached and exceeded, the distributions not only shift toward smaller \( z \), as particles become compressed, but also broaden, i.e., become more polydisperse. The smaller particles (Fig. 3) have a polydispersity ratio of standard deviation to mean that increases from roughly 2% to 4% as \( \zeta \) increases from 0 to 2. In contrast, the larger particles (Fig. 4) have negligible polydispersity when uncrowded, but fluctuate significantly in size for \( \zeta \geq 1 \). For both small and large particles, with increasing Hertz pair potential amplitude, the degree of compression and the breadth of polydispersity increase. The reason why the polydispersity distribution broadens with increasing concentration is that compression forces

Normalized probability distributions for the equilibrium swelling ratio are shown in Fig. 3 and 4 over a range of concentrations. Below close packing \( \zeta < 0.74 \), steric (Hertzian) interparticle interactions are sufficiently weak that the particles are not significantly compressed, as reflected by the distributions differing negligibly from the intrinsic dilute-limit distribution [eqn (2)]. With increasing \( \zeta \), as close packing is approached and exceeded, the distributions not only shift toward smaller \( z \), as particles become compressed, but also broaden, i.e., become more polydisperse. The smaller particles (Fig. 3) have a polydispersity ratio of standard deviation to mean that increases from roughly 2% to 4% as \( \zeta \) increases from 0 to 2. In contrast, the larger particles (Fig. 4) have negligible polydispersity when uncrowded, but fluctuate significantly in size for \( \zeta \geq 1 \). For both small and large particles, with increasing Hertz pair potential amplitude, the degree of compression and the breadth of polydispersity increase. The reason why the polydispersity distribution broadens with increasing concentration is that compression forces
particles into a range of sizes in which the curvature of the Flory–Rehner free energy [eqn (1)] with respect to $a$ is weaker than for uncompressed particles. Measurements of particle size in suspensions of microgels whose dry radii have a static polydisperse\(^7\) or bidisperse\(^8\) distribution show that swollen particles have an equilibrium polydispersity that decreases with increasing particle compression. Conversely, our study demonstrates that microgels whose dry radius is monodisperse have swollen polydispersity – associated purely with fluctuations in swelling ratio – that increases with particle compression.

Particle compressibility is illustrated further in Fig. 5, which plots the volume fraction $\phi$ vs. generalized volume fraction $\zeta$ for suspensions of compressible microgels with $\chi = 0$ and (a) $a_0 = 10$ nm, $a_s = 350.55$ nm, $N_m = 2 \times 10^8$, $N_{ch} = 200$, and (b) $a_0 = 100$ nm, $a_s = 350.55$ nm, $N_m = 2 \times 10^8$, $N_{ch} = 2 \times 10^6$, for various values of Hertz pair potential reduced amplitude $\epsilon^*$. The line $\phi = \zeta$ is drawn for reference. With increasing $\zeta$, self-crowding compresses particles beyond close packing, causing $\phi$ to increase more slowly than $\zeta$.

For $\zeta > 0.74$, the density at which nearest-neighbor particles in the fcc crystal would begin to overlap. For these systems, significant particle compression occurs only in the solid phase. Moreover, the higher the Hertz pair potential amplitude – for given values of $N_m$, $N_{ch}$, and $\chi$ in the Flory–Rehner free energy – the more easily the particles yield to compression.

To explore the evolution of structure as a function of density and interparticle interactions, and to aid our diagnosis of the liquid–solid phase transition, we computed radial distribution functions and static structure factors, as described in Section 3. Fig. 6 shows our results for $g(r)$ over a range of densities that span the freezing transition. The emergence of distinct peaks signals the onset of crystallization at $\zeta \approx 0.58$ for $a_0 = 10$ nm and $\zeta \approx 0.49$ for $a_0 = 100$ nm (black curves in Fig. 6). For both particle sizes, the freezing density is insensitive to $\epsilon^*$ over the range of values considered. Suspensions of larger microgel particles thus crystallize at the same volume fraction as the hard-sphere fluid, while suspensions of smaller nanogel particles remain fluid up to significantly higher volume fractions.
This interesting difference in phase stability can be attributed to the relatively softer Hertz pair repulsion between the smaller particles.

Fig. 7 shows corresponding results for $S(q)$, computed using eqn (7) by averaging over the same configurations used to compute $g(r)$ in Fig. 6. With increasing density, the peaks progressively sharpen and shift toward larger $q$. At the densities at which distinct peaks in $g(r)$ indicate crystallization, the main peak of $S(q)$ attains a height in the range $S(q_{\text{max}}) = 2.8–3$. This freezing threshold is consistent with the Hansen–Verlet

![Fig. 6 Radial distribution functions $g(r)$ vs. radial distance $r$ (in units of uncrowded swollen radius $a_s$) of microgel suspensions, of generalized volume fractions $\zeta$ straddling freezing transition (black curves), with same particle parameters as in Fig. 5 and Hertz pair potential reduced amplitudes (a) $\varepsilon^* = 1.5 \times 10^3$, (b) $\varepsilon^* = 1.5 \times 10^4$, and (c) $\varepsilon^* = 10^7$. Red and blue curves correspond to fluid and solid phases, respectively.](image)

![Fig. 7 Static structure factors $S(q)$ vs. scattered wave vector magnitude $q$ [from eqn (7)] corresponding to radial distribution functions in Fig. 6. Freezing occurs when main peak height $S(q_{\text{max}})$ > 2.8 (black curves). Red and blue curves correspond to fluid and solid phases, respectively.](image)
criterion for fluids interacting via a Lennard-Jones pair potential,\textsuperscript{72} according to which \( S(q_{\text{max}}) \approx 2.85 \) at freezing. In passing, we note that a different freezing criterion proposed specifically for ultrashort pair-potential fluids\textsuperscript{73} does not apply here, since the Hertz pair potential, although bounded, has amplitudes in our system that far exceed the thermal energy \( k_B T \). As a consistency check, we also computed the Lindemann parameter \( L \), defined as the ratio of the root-mean-square displacement of particles from their equilibrium lattice sites to the lattice constant, and confirmed that \( L < 0.15 \) and remains constant in the solid phase.

Finally, we turn to the osmotic pressure, which we computed from our simulations using eqn (8). Fig. 8 presents plots of osmotic pressure vs. generalized volume fraction (equation of state) for the two microgel systems studied. In the dilute regime, the osmotic pressure is very close to that of the hard-sphere fluid, which is consistent with the swelling ratio results (Fig. 5).

![Figure 8](image)

**Figure 8** Equation of state: reduced osmotic pressure \( \Pi_{\text{osm}} \) vs. generalized volume fraction \( \zeta \) [from eqn (8)] for suspensions of compressible microgels with \( \chi = 0 \) and (a) \( a_0 = 10 \text{ nm} \), \( \epsilon^* = 1.5 \times 10^4 \), \( \epsilon^* = 1.5 \times 10^3 \) and (b) \( a_0 = 100 \text{ nm} \), \( \epsilon^* = 10^7 \), \( \epsilon^* = 10^6 \), for various values of Hertz pair potential reduced amplitude \( \epsilon^* \). Insets display broader ranges of \( \zeta \) and \( \pi \). Pressure of hard-sphere fluid \( (\epsilon^* \to \infty) \) is shown for reference. With increasing \( \epsilon^* \), osmotic pressure becomes more hard-sphere-like.

At volume fractions above 20\%, deviations emerge and steadily grow with increasing volume fraction. The compressible microgels have osmotic pressures consistently lower than for the hard-sphere fluid. At volume fractions approaching close packing, the microgel osmotic pressure rapidly rises, yet remains finite beyond close packing, in sharp contrast to the hard-sphere fluid, whose pressure diverges at close-packing. Furthermore, as is clear from Fig. 8a, the osmotic pressure rises more gradually with concentration the smaller and softer the particles. This equilibrium trend may have implications for rheological properties, such as shear viscosity. In fact, recent measurements\textsuperscript{74} of the zero-shear viscosity of aqueous suspensions of monodisperse, highly branched, phytoglycogen nanoparticles\textsuperscript{75} are consistent with significant compression of the particles.

At the apparent freezing density of the microgel suspensions, as diagnosed by the main peak height of the static structure factor, the osmotic pressure plateaus, consistent with a thermodynamic phase transition between fluid and solid. Thus, the freezing behavior of the compressible microgels modeled here seem to be accurately described by the Hansen–Verlet criterion. Our methods are not suited, however, to identifying a glass transition, which could preempt crystallization.

Finally, to probe the dependence of system properties on solvent quality, we repeated several of the calculations for \( \chi = 0.5 \), modeling a theta solvent. As \( \chi \) increases, the particles become progressively compressed, as would be expected with worsening solvent quality, and exert lower osmotic pressure. However, with varying concentration, the systems display similar qualitative trends in polydispersity, volume fraction, structure, and osmotic pressure.

### 5 Conclusions

In summary, we designed and implemented Monte Carlo computer simulations of model suspensions of compressible, soft, spherical, colloidal particles that fluctuate in size and interact via an elastic Hertz pair potential. For this purpose, we introduced a novel trial move that allows particles to expand and contract, according to the Flory–Rehner free energy of cross-linked polymer networks, in response to interactions with neighboring particles. From a series of simulations over ranges of particle parameters chosen to be consistent with experimental systems, we analyzed the dependence of interparticle correlations and thermodynamic behavior on particle size (dry radius) and softness (elastic modulus) by computing a variety of thermal and structural properties.

Radial distribution functions, static structure factors, and osmotic pressures all display behavior similar to that of a hard-sphere fluid at low densities – volume fractions below about 0.3 – but reveal the particles’ intrinsically soft nature at higher densities. Swelling ratios confirm that, with increasing density above close packing, the particles become progressively compressed and polydisperse, compared with their dilute (uncrowded) states. While suspensions of relatively large, stiff particles (microgels of dry radius 100 nm) crystallize at the same volume fraction as a...
fluid of hard spheres, internal degrees of freedom associated with particle compressibility and size polydispersity enable suspensions of smaller, softer particles (nanogels of dry radius 10 nm) to remain in a stable fluid phase up to densities significantly beyond freezing of the hard-sphere fluid. For both nanogels and microgels, the freezing transition is accurately predicted by the Hansen–Verlet criterion.

Our calculations of equilibrium swelling ratios and bulk osmotic pressures are qualitatively consistent with observations of significant compression of deformable particles, albeit icosahedral microgels, only at volume fractions approaching and exceeding close packing.17,24 Similarly, our finding that particle softness lowers the osmotic pressure is consistent with experimental measurements of reduced zero-shear viscosity in suspensions of soft nanoparticles.74 Furthermore, our calculations may guide the choice of system parameters in future experiments and molecular-scale simulations and could be extended to map out equilibrium phase diagrams.

The coarse-grained model of nonionic, spherical microgels studied here may be refined by incorporating a more realistic swelling free energy66 that goes beyond the limitations of the Flory–Rehner theory noted in Section 2.1, and may be further developed in several directions. For example, the model may be extended to ionic microgels, whose properties emerge from an interplay between elastic and electrostatic interparticle interactions. Such an extension would enable analyzing the coupled influences of fluctuating particle size and counterion distribution on swelling, structure, and phase behavior of concentrated suspensions of soft, charged colloids. By incorporating shape fluctuations, our simulation method also may be generalized to model dynamically deforming particles, as in recent studies of elastic colloids,50–62 and extended to study the influence of added hard crowders, as in our previous studies of polymer–nanoparticle mixtures.64–66 Finally, rheological properties, such as diffusion coefficients, viscosity, elastic moduli, jamming and glass transition densities69 could be explored by wedging our model of soft, compressible, size-fluctuating colloids to appropriate simulation methods, such as Brownian dynamics, lattice Boltzmann, or molecular dynamics of micromechanical models.69,62

Acknowledgements

This work was partially supported by the National Science Foundation (Grant No. DMR-1106331).

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