Is molecular gas necessary for star formation?

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ABSTRACT
On galactic scales, the surface density of star formation appears to be well correlated with the surface density of molecular gas. This has led many authors to suggest that there exists a causal relationship between the chemical state of the gas and its ability to form stars – in other words, the assumption that the gas must be molecular before star formation can occur. We test this hypothesis by modelling star formation within a dense cloud of gas with properties similar to a small molecular cloud using a series of different models of the chemistry, ranging from one in which the formation of molecules is not followed and the gas is assumed to remain atomic throughout, to one that tracks the formation of both H₂ and CO. We find that the presence of molecules in the gas has little effect on the ability of the gas to form stars: star formation can occur just as easily in atomic gas as in molecular gas. At low densities (<10⁴ cm⁻³), the gas is able to cool via C⁺ fine-structure emission almost as efficiently as via CO rotational line emission, while at higher densities, the main cooling process involves the transfer of energy from gas to dust, meaning that the presence of molecules is again unimportant. Cooling by H₂ is particularly inefficient, accounting for as little as 1 per cent of the overall cooling in the cloud. Rather than the chemical makeup, we find that the most important factor controlling the rate of star formation is the ability of the gas to shield itself from the interstellar radiation field. As this is also a prerequisite for the survival of molecules within the gas, our results support a picture in which molecule formation and the formation of cold gas are both correlated with the column density of the cloud – and thus its ability to shield itself – rather than being directly correlated with each other.

Key words: stars: formation – ISM: clouds – ISM: molecules – galaxies: ISM.

1 INTRODUCTION
Essentially all Galactic star formation occurs within dense clouds of molecular gas, known as molecular clouds (MCs). Furthermore, recent observations have demonstrated that on large scales within local galaxies, there is a surprisingly close correlation between the surface density of star formation, Σ_{SFR}, and the surface density of molecular hydrogen, Σ_H₂ (see e.g. Wong & Blitz 2002; Bigiel et al. 2008, 2011; Leroy et al. 2008). An obvious interpretation of these observations is that the formation of stars depends on the presence of molecular gas (Krumholz & McKee 2005; Elmegreen 2007; Krumholz, McKee & Tumlinson 2009). However, it is not immediately obvious why this should be the case. Although H₂ can be an important coolant of interstellar gas (Gnedin & Kravtsov 2011), it is effective only at temperatures of a few hundred Kelvin or higher. At the temperatures typical of gas within MCs (T ~ 10–20 K), the H₂ cooling rate is tiny, and hence H₂ cannot play a direct role in enabling the gas to cool, undergo gravitational collapse and form stars.

A more promising route by which H₂ can influence the thermodynamics of the gas is through the fact that its presence is required for the efficient formation of carbon monoxide (CO). Unlike H₂, CO can provide effective cooling even in very low temperature gas, and it is generally found to be the dominant gas-phase coolant within pre-stellar cores (Neufeld, Lepp & Melnick 1995; Goldsmith 2001). However, even if the H₂ and CO were absent, the gas would still be able to cool to low temperatures through fine-structure emission from ionized and neutral atomic carbon. In previous modelling, we have shown that C⁺ cooling alone can reduce the gas temperature to T ~ 20 K within gas that is shielded from the effects of photoelectric heating by dust extinctions of A_V ~ 1–2 or more (Glover & Mac Low 2007). To reduce the temperature further, to the 10 K typical of most pre-stellar cores, a molecular coolant such as CO is still required, but it seems unlikely that the difference between the ~10 K temperatures reachable with molecular cooling and the ~20 K temperatures reachable with atomic fine-structure cooling can have any great effect on the ability of gas to form stars.

One is therefore led to ask whether the presence of molecules is truly essential for star formation. Perhaps the reason that we find such a good correlation between molecular gas and star formation is not that molecular gas is a prerequisite for star formation, but...
instead that the formation of molecules and the formation of stars both correlate with some other factor, such as the existence of large, dense clouds of gas. In this picture, the molecules are a consequence, not a cause, of the conditions required to form stars.

To help us better understand whether or not the presence of molecular gas is a necessary condition for star formation, we have performed a number of numerical simulations of the formation of stars in a dense cloud of gas with properties similar to a small MC. We use a range of different models of the chemistry and thermal balance of the gas to explore the influence that molecule formation and dust shielding have on the ability of the cloud to form stars. In Section 2, we discuss the numerical set-up that we use to perform these simulations, and our choice of initial conditions. The results are presented in Section 3, and in Section 4 we discuss what these results imply for the nature of the link between molecular gas and star formation. We conclude in Section 5.

2 SIMULATIONS

2.1 Numerical approach

Our simulations were performed using a modified version of the GADGET 2 smoothed particle hydrodynamics (SPH) code (Springel 2005). Our modifications include a sink particle algorithm for treating gravitationally collapsing regions that become too small to resolve (Bate, Bonnell & Price 1995), the inclusion into the equation of motion of an optional confining pressure term (Benz 1990), a treatment of gas-phase chemistry (described in more detail below), as well as radiative heating and cooling from a number of atomic and molecular species (Glover & Jappsen 2007; Glover et al. 2010; Glover & Clark 2011), and an approximate treatment of the attenuation of the Galactic interstellar radiation field (ISRF). The effects of magnetic fields are not included.

In order to establish the role that molecular cooling plays in determining the star formation rate, we have run a series of simulations in a small, dense gas cloud with properties similar to those of a small MC, using several different treatments of the cooling and chemistry of the gas. In our least realistic model (run A), we include the simple network for hydrogen chemistry described in Glover & Mac Low (2007), together with the model for CO chemistry developed by Nelson & Langer (1997), but we assume that the gas remains optically thick throughout the simulation, i.e. we neglect any attenuation of the ISRF by dust absorption or molecular self-shielding. In practice, this means that the gas remains in atomic form at all but the highest densities (see Section 3.2). In run B, we include the effects of dust absorption, but ignore the chemical evolution of the gas, forcing it to remain in atomic form throughout.

To model the dust absorption, we use our new Treecol algorithm, as described in more detail in Section 2.2. In run C, we include the simple network for hydrogen chemistry described in Glover & Mac Low (2007), but assume that the carbon and oxygen in the gas remain as C\(^+\) or O, respectively. In this model, the only molecular cooling comes from H\(_2\). Finally, in runs D1, D2 and D3, we include both the Glover & Mac Low (2007) hydrogen chemistry and the Nelson & Langer (1997) CO chemistry, this time including the effects of dust absorption and self-shielding. This set-up has been shown to produce more CO than would be the case with more detailed chemical treatments (Glover & Clark 2011), and hence gives us a reasonable upper bound on the effectiveness of CO cooling. We performed three simulations using this treatment of the chemistry: one in which the hydrogen is initially atomic (run D1), and two in which it is initially molecular (runs D2, D3). These final two runs differ only in the numerical resolution adopted: run D2 is performed using our standard resolution (discussed in Section 2.4), while run D3 is performed using 10 times more SPH particles, and hence has 10 times better mass resolution. A brief summary of these models is given in Table 1.

None of the models that we study in this paper includes the effects of freeze-out of species such as CO on to dust grains. However, we do not expect this simplification to significantly affect the thermal balance of the cloud (see e.g. Goldsmith 2001).

2.2 Attenuation of the ISRF

We assume that our model clouds are illuminated by the standard ISRF, using the parametrization from Draine (1978) in the ultraviolet (UV), and from Black (1994) at longer wavelengths. To model the effects of extinction, H\(_2\) self-shielding, CO self-shielding and the shielding of CO by H\(_2\), we use the Treecol algorithm (Clark et al. 2011). This algorithm allows us to approximate the distribution of column densities (of hydrogen nuclei, molecular hydrogen or CO) seen by each particle by using information stored in the oct-tree that is also used in the GADGET 2 code to compute gravitational accelerations. Our current implementation of Treecol uses the HEALPIX pixelation scheme (Górski et al. 2005) and yields for each SPH particle a 4\(\pi\) sr projection of the column density distribution seen by that particle, discretized into 48 equal-area HEALPIX pixels.

To illustrate how we can use this pixelated projection to compute photoheating or photodissociation rates for a given SPH particle, let us follow how we would go about computing the photoelectric heating rate. We begin with the appropriate pixelated column density distribution, which in this case is that for the column density of hydrogen nuclei in all forms, \(N_{H,\text{col}}\). We use the relationship \(A_V = 5.348 \times 10^{-22}(N_{H,\text{col}}/1\ \text{cm}^{-2})\) between \(N_{H,\text{col}}\) and the visual extinction \(A_V\) (Bohlin, Savage & Drake 1978; Draine & Bertoldi 1996) to associate a visual extinction with each pixel. We next compute an attenuation factor \(f_{pe}\) for each pixel, which we define as \(f_{pe} = \Gamma_{pe}(A_V)/\Gamma_{pe}(0)\), where \(\Gamma_{pe}(A_V)\) is the photoelectric heating rate in gas with a visual extinction equal to \(A_V\), and \(\Gamma_{pe}(0)\) is the photoelectric heating rate in the optically thin limit. We take our expressions for these quantities from Bergin et al. (2004). Finally, once we have computed \(f_{pe}\) for each pixel, we make use of the fact that the HEALPIX pixels have equal areas to compute a mean attenuation factor \(\langle f_{pe}\rangle\) for the gas represented by the SPH particle by averaging \(f_{pe}\) over all pixels. The photoelectric heating rate in this gas is then \(\Gamma_{pe} = \langle f_{pe}\rangle \Gamma_{pe}(0)\).

We use the same strategy to compute the rate at which dust is heated by the ISRF, taking our expression for the dependence of the heating rate on \(A_V\) from Glover & Clark (2011). We also use a similar strategy to compute the \(\Gamma_{H_2}\) and CO photodissociation rates.
However, in this case it is necessary to use the Treecol algorithm to compute the distributions of H$_2$ and CO column densities in addition to the total hydrogen column density, since these are needed in order to compute the mean attenuation factors for H$_2$ self-shielding, $\langle f_{H_2,H_2} \rangle$, CO self-shielding, $\langle f_{CO,CO} \rangle$, and the shielding of CO by H$_2$, $\langle f_{H_2,CO} \rangle$. Our expression for $f_{H_2,H_2}$ comes from Draine & Bertoldi (1996), while those for $f_{H_2,CO}$ and $f_{CO,CO}$ come from Lee et al. (1996). A more accurate treatment of CO self-shielding and the shielding of CO by H$_2$ has recently been given by Visser, van Dishoeck & Black (2009), but we would not expect our results to change significantly if we were to use this in place of the older Lee et al. (1996) treatment.

2.3 Sink particles
Sink particles are formed once the gas exceeds a number density of $10^7$ cm$^{-3}$, which is around the density at which we start to lose resolution in the $2 \times 10^6$ particle simulations (assuming a minimum temperature of 8 K; see Section 3.2). To ensure that sink particles are not created by mistake, we require the parcel of gas comprising the candidate particle and its 50 nearest neighbours to be gravitationally bound and collapsing (following the prescription given by Bate et al. 1995). Once formed, sink particles are accreted into. The starting point for our calculations is a uniform sphere with a hydrogen nuclei number density $n = 300$ cm$^{-3}$, and a total mass of $10^6$ M$_\odot$, meaning that it has an initial radius of approximately 6 pc. Such conditions are typical of those found in nearby star-forming clouds, and give the cloud a visual extinction at its centre of roughly 3. We model the cloud with either $2 \times 10^6$ SPH particles (our standard resolution) or $2 \times 10^7$ SPH particles (our high resolution, used only in run D3), and we require that the physical quantities for every SPH particle are calculated by averaging over 50 neighbours. This sets the mass resolutions at 0.5 and 0.05 M$_\odot$ in our low- and high-resolution simulations, respectively (Bate & Burkert 1997). We inject bulk (non-thermal) motions into the cloud by imposing a turbulent velocity field that has a power spectrum of $P(k) \propto k^{-4}$. The energy in the turbulence is initially equal to the gravitational energy in the cloud, giving an initial root-mean-squared velocity of around 3 km s$^{-1}$. The turbulence is left to freely decay via shocks and compression-triggered cooling. We set the initial temperature of the gas to 20 K, but this is quickly altered when the simulation starts, as the gas tries to find an equilibrium between the various heating and cooling processes that are included in our model of the interstellar medium (ISM). We adopt a confining pressure equal to $P_{\text{ext}} = 12,000$ K cm$^{-3}$, but note that runs with much smaller values of $P_{\text{ext}}$ produce very similar results. 

We adopt total carbon and oxygen abundances relative to hydrogen that are $x_C = 1.4 \times 10^{-4}$ and $x_O = 3.2 \times 10^{-4}$, respectively (Sembach et al. 2000). For the cosmic ray ionization rate of atomic hydrogen, we take a value $\zeta_H = 10^{-15}$ s$^{-1}$. Cosmic ray ionization rates for other species (e.g. molecular hydrogen) were computed assuming that they had the same ratios to $\zeta_H$ as given in the UMIST99 chemical data base (Le Teuff, Millar & Markwick 2000).

3 RESULTS

3.1 Star formation in the clouds
In the top panel of Fig. 1, we show the rate at which mass is converted into sink particles in runs B, C, D1 and D2. In all four of these runs, star formation begins within the cloud after roughly 2–2.5 Myr. For comparison, the global free-fall time of the cloud in its initial state is approximately 2.5 Myr, and so in all four of these runs, stars begin to form within roughly one free-fall time. If we look in more detail at the time histories plotted in Fig. 1, we see that the time that elapses between the beginning of the simulations and the onset of star formation has a slight sensitivity to the chemical state of the gas. Run D2, which includes both H$_2$ and CO chemistry, and which begins with the hydrogen already fully molecular, is the first run to begin forming stars. However, star formation in run C (initially atomic, H$_2$ chemistry only) and run D1 (initially atomic, H$_2$ and CO chemistry) is delayed only slightly compared to run D2, by roughly 0.1 Myr. Moreover, by the end of the simulation, all three simulations are forming stars at very nearly the same rate, although a greater number of stars have formed in run D2, owing to its head start. Finally, star formation in run B (atomic gas) is delayed for slightly longer, roughly 0.3 Myr, although once star formation does begin, it occurs at a very similar rate to that in the other three runs.
Nevertheless, the differences between the star formation histories of the clouds simulated in these four runs are relatively small, despite the significant differences that exist in the chemical make-up of the clouds. The presence of H$_2$ and CO within the gas appears to make only a small difference in the ability of the cloud to form stars. Furthermore, the fact that a cloud that does not form any molecules is not only able to form stars, but does so with only a short delay compared to one in which all of the hydrogen and a significant fraction of the carbon is molecular is persuasive evidence that the formation of molecules is not a prerequisite for the formation of stars.

Examination of the nature of the stars formed in these four simulations is also informative. Naively, one might expect that in the absence of molecular cooling, or more specifically CO cooling, the minimum temperature reached by the star-forming gas would be significantly higher. If so, then this would imply that the value of the Jeans mass in gas at this minimum temperature would also be significantly higher. It has been argued by a number of authors (e.g. Jappsen et al. 2005; Larson 2005; Bonnell, Clarke & Bate 2006) that it is the value of the Jeans mass at the minimum gas temperature in a star-forming cloud that determines the characteristic mass in the resulting initial mass function (IMF). Following this line of argument, one might therefore expect the characteristic mass to be much higher in clouds without CO. However, our results suggest that this is not the case. In runs C, D1 and D2, the mean mass of the stars that form is roughly 1–1.5 M$_\odot$ (Fig. 1, bottom panel) and shows no clear dependence on the CO content of the gas. Indeed, the mean mass is slightly lower in run C, which has no CO, than in run D2, which does. The mean stellar mass that we obtain from these simulations is slightly higher than the characteristic mass in the observationally determined IMF, which is typically found to be somewhat less than a solar mass (Chabrier 2001; Kroupa 2002). However, this is a consequence of our limited mass resolution, which prevents us from forming stars less massive than 0.5 M$_\odot$, and hence biases our mean mass towards higher values. (We return to this point in Section 3.3.) In run B, we again find a greater difference in behaviour, but even in this case, the mean stellar mass remains relatively small, at roughly 2 M$_\odot$. It therefore appears that the presence or absence of molecules does not strongly affect either the star formation rate of the clouds or the mass function of the stars that form within them.

Conspicuous by its absence from our discussion so far has been run A, the run in which we assumed that the gas remained optically thin throughout the simulation. In this run, we find a very different outcome. Star formation is strongly suppressed, and the first star does not form until $t = 7.9$ Myr, or roughly three global free-fall times after the beginning of the simulation. The results of this run suggest that it is the ability of the cloud to shield itself from the effects of the ISRF, rather than the formation of molecules within the cloud, that plays the most important role in regulating star formation within the cloud (cf. Krumholz, Leroy & McKee 2011).

### 3.2 Thermal and chemical state of the gas

#### 3.2.1 Temperature distribution

In order to understand why molecular gas appears to be of only very limited importance in determining the star formation rate, it is useful to look at the thermal state of the gas in the different runs at the point at which they begin forming stars. This is illustrated in Fig. 2 for runs B, C, D1 and D2. For comparison, we also show the temperature distribution of the gas in run A at $t = 2.3$ Myr (i.e. at a similar time to the other four runs, albeit roughly 5.6 Myr before run A itself begins to form stars). The first point to note is the basic similarity of the temperature distribution in most of the runs. In runs B, C, D1 and D2, the temperature decreases from roughly 100 K at $n \sim 10^3$ cm$^{-3}$ to 10 K at $n = 10^5$ cm$^{-3}$ and to 8 K at $n = 10^6$ cm$^{-3}$. This corresponds to a relationship between temperature and density that can be approximated as $T \propto \rho^{-0.25}$ at $n < 10^5$ cm$^{-3}$, or a relationship between pressure and density $P \propto \rho^{0.75}$, in good agreement with the relationship $P \propto \rho^{0.73}$ proposed by Larson (1985, 2005). The fact that the effective equation of state of the gas is significantly softer than isothermal (i.e. $P \propto \rho$) means that the local Jeans mass decreases rapidly with increasing density within the cloud, a factor which is known to greatly assist gravitational fragmentation (see

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**Figure 2.** Gas temperature plotted as a function of $n$, the number density of hydrogen nuclei, in runs B, C, D1 and D2 (panels 2–5) at a time immediately prior to the onset of star formation in each of these runs. Note that this means that each panel corresponds to a slightly different physical time. For comparison, we also plot the temperature of the gas as a function of density in run A (panel 1, at the top) at a similar physical time, $t = 2.3$ Myr, although in this case, this is long before the cloud begins to form stars.
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Figure 3. Comparison of the mass-weighted density PDF in the various runs. For runs B, C, D1 and D2, we show the state of the gas immediately prior to the onset of star formation, while for run A, we show the state of the gas at a similar physical time, \( t = 2.3 \) Myr.

e.g. Li, Klessen & Mac Low 2003; Jappsen et al. 2005; Clark, Glover & Klessen 2008; Dopcke et al. 2011). In run A, on the other hand, there is a brief period of cooling at low densities, but the gas then begins to reheat at densities \( n > 500 \) cm\(^{-3}\), and the temperature in the densest gas is higher than the temperature at the edge of the cloud. It is therefore not surprising that gravitational fragmentation is strongly suppressed in this run.

If we look in more detail at the relationship between temperature and density in the four runs that do show significant cooling, then several additional features become apparent. First, all of the runs show a significant degree of scatter in the relationship at densities between \( n \sim 100 \) and \( \sim 10^4 \) cm\(^{-3}\) (in run B) or \( n \sim 10^5 \) cm\(^{-3}\) (in the other runs), but this scatter abruptly vanishes at higher densities. This pronounced change in behaviour is due in part to a change in the dominant coolant within the clouds. At low densities, gas-phase coolants (primarily \( \text{C}^+ \) and CO) dominate, while at higher densities, energy transfer between gas and dust becomes the dominant process regulating the gas temperature. In the regime dominated by gas-phase cooling, the local cooling rate depends on the local value of the optical depth in the appropriate cooling line, and hence on the local details of the velocity structure of the cloud. In the dust-dominated regime, on the other hand, the gas temperature quickly converges to the dust temperature, which is determined largely by continuum emission and absorption and which is thus insensitive to the velocity structure of the cloud. In addition, another effect contributing to the scatter at low densities is the sensitivity of the photoelectric heating rate to the visual extinction. We know from previous work that the mean visual extinction within a given fluid element in a turbulent cloud is only poorly correlated with the volume density of the cloud (Glover et al. 2010), and hence the value of the photoelectric heating rate shows a significant scatter at any given density. At low densities, photoelectric heating is the dominant heat source (see Section 3.2.4), and so this scatter in the heating rate helps to create a significant scatter in the gas temperature. At higher densities, photoelectric heating becomes far less important, and so the scatter in the photoelectric heating rate has much less effect on the temperature.

A second feature to note is the pronounced ‘hump’ in the temperature–density distribution, roughly centred at \( T \sim 20 \) K and \( n \sim 2 \times 10^4 \) cm\(^{-3}\), that is present in runs C and D1, but absent in runs B and D2. This feature is caused by \( \text{H}_2 \) formation heating: we assume (following Takahashi & Uehara 2001) that \( \text{H}_2 \) molecules form on dust grains with a high degree of rotational and vibrational excitation, and at densities above a few thousand particles per cubic centimetre, much of this energy is converted into thermal energy by collisional de-excitation of the newly formed \( \text{H}_2 \) molecules. This does not occur in run B because no \( \text{H}_2 \) is allowed to form in that run, and it does not occur in run D2 because the hydrogen starts in fully molecular form, and although some is subsequently dissociated, the atomic hydrogen fraction at the appropriate densities remains small (see Fig. 4).

Figure 4. Fractional abundance of \( \text{H}_2 \) (defined as the ratio of the \( \text{H}_2 \) number density \( n_{\text{H}_2} \) and the number density of hydrogen nuclei, \( n \)), plotted as a function of \( n \), for runs A, C, D1 and D2. With this definition of the fractional abundance, a value of 0.5 corresponds to fully molecular gas. For runs C, D1 and D2, we show the state of the gas immediately prior to the onset of star formation, while for run A, we show the state of the gas at a similar physical time, \( t = 2.3 \) Myr.
Finally, the influence of the CO in runs D1 and D2 is clear if we look at the temperature distribution of the gas at densities of around $10^3$ to $10^4$ cm$^{-3}$. The minimum gas temperature reached in the runs with CO is approximately 5 K, roughly half the size of the minimum temperature reached in the runs that must rely on C$^+$ cooling. However, despite the fact that the gas is able to reach lower temperatures in the runs with CO cooling, very little of it does so: most of the gas at these densities has a temperature that is close to 10 K, implying that the difference in the mean temperature of the gas is much smaller than the difference in the minimum temperature.

Given the similarity between the temperature distribution in run B and that in runs C, D1 and D2, it may at first seem odd that star formation in the former is delayed by roughly 0.3 Myr compared to star formation in the latter, and that the mean mass of the stars that form is noticeably smaller. However, this has a simple explanation. At a given density and temperature, the Jeans mass scales with the mean molecular weight $\mu$ as $M_J \propto \mu^{-3/2}$. In run B, the gas is fully atomic at all densities, and so $\mu = 1.27$ amu (where we have assumed a helium fraction of 0.1 by number, relative to hydrogen). On the other hand, in runs C, D1 and D2, the hydrogen in the densest gas is almost fully molecular, as illustrated in Fig. 4, and so $\mu = 2.33$ amu. Therefore, for any given choice of density and temperature within the dense gas, the Jeans mass is roughly a factor of 2.5 times larger in run B than in runs C, D1 or D2. If we assume that gas is assembled into dense filaments and cores at roughly the same rate in all of these runs, which seems likely given the similar temperature–density relationship, then this implies that in run B it will take longer for these structures to grow to the point at which they become gravitationally unstable, and hence that the onset of star formation will be delayed. It also suggests that the stars that do form will have systematically larger masses, in agreement with what we find in our simulations.

### 3.2.2 Density distribution

We can gain additional insight into the physical processes determining the star formation rate in our model clouds by examining the probability density function (PDF) of gas density generated in the different runs. In Fig. 3, we show the mass-weighted density PDF of the gas in runs B, C, D1 and D2 immediately prior to the onset of star formation in these four runs. For comparison, we also show the density PDF in run A at a similar physical time, $t = 2.3$ Myr.

In the four star-forming runs, the density PDF is broad, and shows evidence for a power-law tail at high densities, $n > 10^4$ cm$^{-3}$. Similar features have been found in previous simulations of self-gravitating supersonic turbulence (e.g. Klessen 2000; Federrath et al. 2008a; Kritsuk, Norman & Wagner 2011), in which run-away gravitational collapse has occurred. There is also new observational evidence for the presence of power-law tails in the density PDFs of active star-forming regions in real MCs (Kainulainen et al. 2009, 2011; Lombardi, Lada & Alves 2010). In contrast, the density PDF in run A is much narrower, and appears to have a lognormal form, as would be expected in a cloud in which gravitational collapse has not yet occurred. The higher gas temperatures in run A compared to the other runs mean that the turbulence has a much smaller root-mean-squared Mach number, and hence produces weaker compressions, leading to a significantly narrower PDF (Padoan, Nordlund & Jones 1997; Federrath, Klessen & Schmidt 2008b; Padoan & Nordlund 2011). As a result, none of the gas in run A has yet reached a high enough density to become locally self-gravitating and to decouple from the larger scale flow, while in the other four runs, a significant fraction of the gas mass is found in collapsing, self-gravitating structures.

The fact that the four star-forming runs have very similar density PDFs is a consequence of the fact that they have very similar temperature distributions. It is therefore easy to understand why they form stars at very similar rates: in all four cases, the amount of dense gas available for star formation is very similar, and the rate at which this dense gas is converted into stars is limited primarily by the local free-fall time, which does not depend upon the nature of the gas coolants.

### 3.2.3 Molecular abundances

In Fig. 4, we plot the fractional abundance of H$_2$, $x_{H_2}$, as a function of the hydrogen nuclei number density $n$ in runs C, D1 and D2 at a time shortly before the onset of star formation in these simulations. For comparison, we also plot $x_{H_2}$ versus $n$ at a similar output time in run A. We show no results from run B because $x_{H_2} = 0$ by design in this run. We define $x_{H_2}$ as the ratio of the H$_2$ number density $n_{H_2}$ and the hydrogen number density $n$, which means that in fully molecular gas, $x_{H_2} = 0.5n/n = 0.5$.

If we compare the results from runs C, D1 and D2, we see that in each case, the cloud is predominantly molecular at the point at which it forms stars. The mean H$_2$ fractional abundance falls significantly below 0.5 only for densities $n < 100$ cm$^{-3}$, corresponding to warm, unshielded gas at the boundaries of the clouds. The rapidity with which H$_2$ forms within the clouds is a consequence of the many transient density enhancements produced by the supersonic turbulence, which boost the overall H$_2$ formation rate in the cloud by a factor of a few (for more details, see e.g. Glover & Mac Low 2007; Mac Low & Glover 2011; Milosavljevic et al. 2011). The main difference between runs C, D1 and D2 is the larger scatter in $x_{H_2}$ at high densities in runs C and D1 than in run D2. This reflects the difference in initial conditions between these runs: runs C and D1 start with all of their hydrogen in atomic form, and although most of it has become molecular by $t \sim 2.5$ Myr there are still a few regions that retain a high atomic fraction. In run D2, on the other hand, the hydrogen is initially in fully molecular form, and atomic hydrogen is produced only by photodissociation. The main conclusion that we can draw from this is that at the point at which star formation begins, the clouds have not yet reached chemical equilibrium throughout their volume.

In run A, on the other hand, the situation is very different. In the absence of H$_2$ self-shielding and dust shielding, the H$_2$ fractional abundance is much smaller: the peak value at the displayed output time of 2.3 Myr is $x_{H_2} \simeq 2 \times 10^{-3}$, implying that even in the densest gas, less than 1 per cent of the hydrogen is in molecular form. In addition, the very small degree of scatter in the relationship between $x_{H_2}$ and $n$ implies that the gas is in chemical equilibrium, as we would expect given that in the absence of shielding, the H$_2$ photodissociation time-scale $t_{pd} \simeq 600$ yr, which is very much shorter than the age of the cloud.

In Fig. 5, we show how the fractional abundance of CO, $x_{CO} \equiv n_{CO}/n$, varies as a function of $n$ in runs A, D1 and D2. Results are shown at the same output times as in Fig. 4. No results are plotted for runs B or C, because $x_{CO} = 0$ by design in these runs. Several points should be noted. First, the CO abundance in run A is tiny, as is to be expected given the low H$_2$ abundance and the absence of dust shielding. Secondly, the distribution of CO abundances in runs D1 and D2 is very similar, despite the difference in the initial conditions for these two runs. This suggests that the CO content of the gas is primarily sensitive to its current H$_2$ content and density.
3.2.4 Dominant thermal processes

To help us to understand why the presence or absence of molecules appears to have such a limited effect on the temperature structure of the clouds and the progress of star formation within them, it is useful to examine how the dominant heating and cooling process vary with density within an atomic cloud and a MC. We have therefore calculated the median heating/cooling rate as a function of density for each process included in our thermal model for runs B and D2 at a time just before the onset of star formation. The results are plotted in Figs 7 (for run B) and 8 (for run D2). Values are plotted only for the most important processes; minor contributions to the cooling from e.g. $\text{H}^+$ recombination or the collisional ionization of atomic hydrogen are omitted. We have chosen to plot the median values rather than the mean values because the latter are strongly influenced by dissipation in shocks, which occupy a relatively small fraction of the simulation volume but dissipate a significant amount of energy within the shocked regions (see e.g. Pan & Padoan 2009). The median values give a fairer picture of the balance of heating and cooling rates in the bulk of the gas.

Fig. 7 demonstrates that in the atomic cloud, there are three main regimes. At densities $n < 2000 \text{ cm}^{-3}$, the heating of the gas is dominated by photoelectric emission from dust grains, and the cooling is dominated by fine structure emission from $\text{C}^+$. Between $n \sim 2000$ and $\sim 2 \times 10^4 \text{ cm}^{-3}$, $\text{C}^+$ remains the main coolant, but photoelectric heating becomes much less effective, owing to the increasing visual extinction of the cloud at these densities. In this density range, adiabatic compression of the gas (indicated in the plot as the $pdV$ term), dissipation of turbulent kinetic energy in shocks and cosmic ray ionization heating are all significant sources of heat. Finally, at densities greater than $n > 2 \times 10^4 \text{ cm}^{-3}$, the time-scale for energy transfer between gas and dust becomes short enough to couple the gas and dust temperatures together, at which point this (followed by thermal emission from the dust grains) becomes the most important cooling process. Weak shocks and adiabatic compressions together dominate the heating of the gas in this regime, each contributing close to half of the total heating rate.
Fig. 7. Median heating and cooling rates per unit volume in run B, plotted as a function of the hydrogen nuclei number density $n$, at a time just before the onset of star formation.

Fig. 8. As Fig. 7, but for run D2.

Fig. 8 shows that in the MC, a number of additional processes come into play: $H_2$ and CO provide additional cooling channels through their rotational line emission, but the presence of $H_2$ also introduces additional heating processes such as $H_2$ photodissociation heating (Black & Dalgarno 1977), or heating due to the pumping of highly excited vibrational levels of $H_2$ by UV photons (Burton, Hollenbach & Tielens 1990). Nevertheless, despite the additional complexity, we can again identify three main regimes marked out by different dominant processes. At $n < 1000 \, \text{cm}^{-3}$, the behaviour is very similar to that in the atomic run: $C^+$ is the dominant coolant, while most of the heating comes from photoelectric emission from dust. Above $n = 1000 \, \text{cm}^{-3}$, $C^+$ quickly gives way to CO as the dominant coolant, reflecting the fact that the gas becomes CO dominated at around this density (see Fig. 5), and the photoelectric heating rate also begins to fall off with increasing density. The fact that these changes occur at a very similar density is no coincidence: the photoelectric heating rate and the $H_2$ photodissociation rate have a very similar dependence on the visual extinction of the gas, and so both become unimportant at roughly the same point. CO remains the dominant coolant between $n = 1000$ and $10^5 \, \text{cm}^{-3}$, but photoelectric heating quickly becomes irrelevant, and dissipation in shocks becomes the main source of heat. Finally, at $n > 10^5 \, \text{cm}^{-3}$, dust takes over from CO as the most important coolant, and pdV heating becomes almost as important as shock heating.

Fig. 8 also illustrates that cooling by $H_2$ is never particularly important: at best, it contributes only a few per cent of the total cooling rate, and at most densities contributes far less than this. In addition, it demonstrates that $H_2$ formation heating is unimportant in run D2, which is unsurprising given the fully molecular initial conditions used for this run. A similar plot for run D1 would show a much larger contribution from $H_2$ formation heating at densities between $n = 10^3$ and $10^4 \, \text{cm}^{-3}$.

If we compare Figs 7 and 8, we can see why the presence of H$_2$ and CO appears to have such a limited effect on the behaviour of the cloud. Below $n = 1000 \, \text{cm}^{-3}$ (which is, let us not forget, more than three times higher than the initial mean density of the gas), the cooling is dominated by $C^+$ in both simulations, and so $H_2$ and CO have very little influence on the thermal behaviour of the gas. At higher densities, CO takes over from $C^+$ as the dominant coolant in run D2. However, if we compare the CO cooling rate at e.g. $n = 10^5 \, \text{cm}^{-3}$ in run D2 with the $C^+$ cooling rate at the same density in run B, we see that they are surprisingly similar – the $C^+$ cooling rate is smaller than the CO cooling rate, but only by a factor of 2–3, despite the much larger energy required to excite
the C\(^+\) line compared to the CO \(J = 1 \rightarrow 0\) line. It is this fact that ultimately renders the CO inessential: if we were to remove it, the temperature of the gas would rise slightly, and the cooling rate would fall by a factor of a few, but otherwise, the behaviour of the cloud would hardly change, and hence its ability to form stars would not be greatly affected. Since, as we have already seen, H\(_2\) cooling is also unimportant, we can therefore conclude that molecular cooling in general is not required in order to form stars, given the initial conditions examined here. In a realistic model, the gas that forms stars will be molecular (as in runs C, D1 and D2), but even if it were not (as in run B), it would still form stars at almost the same rate.

Finally, we note that although the chemical model used in our simulations does not include atomic carbon, which could potentially be an important low-temperature coolant, we would not expect its inclusion to significantly affect the star formation rate. Atomic carbon is unlikely to provide more cooling at low temperatures than CO, and as we have already seen, the star formation rate is insensitive to the amount of CO present in the gas, implying that the star formation rate will also be insensitive to the ratio of C\(^+\) to C. We have tested this assumption by resimulating the cloud from run D2 using a more detailed chemical model that does include atomic carbon (the NL99 model described in Glover & Clark 2011, which is a slightly modified version of a model first introduced by Nelson & Langer 1999). As expected, we find that the star formation rate in this run is essentially the same as in run D2.

3.3 Influence of numerical resolution

To establish the extent to which our results are affected by the limited mass resolution of our simulations, we performed a single simulation with the same initial conditions and chemical model as run D2, but which had 10 times more SPH particles, and hence a mass resolution of 0.05 M\(_\odot\), 10 times smaller than in our standard runs. We denote this run as D3. In Fig. 9, we compare the growth of the mass incorporated into sink particles, the number of sink particles formed and the mean sink particle mass in runs D2 and D3. We see that the high-resolution run D3 begins to form stars at almost the same point as the lower resolution run D2, and that the stellar mass increases at nearly the same rate, although the much higher computational cost of the higher resolution run means that we are unable to follow the evolution of the system for as long as in the low-resolution run. We also note the high-resolution run forms a significantly larger number of stars than the low-resolution run, with a mean stellar mass that is a factor of a few smaller.

These results suggest that the rate at which stars form within our model clouds is not strongly influenced by the limited mass resolution of our simulations. This is what one would expect if the main factor determining the star formation rate is the formation of self-gravitating, dense cores (see e.g. Kruijssen 2015; Padoan & Nordlund 2011), as most of these cores are well resolved even in our low-resolution simulations. The mass distribution of the stars that form, on the other hand, is sensitive to fragmentation occurring within the cores, which is not well resolved within our low-resolution models, as the differences in the lower two panels of Fig. 9 clearly demonstrate.

We therefore conclude that our major results, which concern the timing and rate of star formation within the different clouds, should be insensitive to our choice of numerical resolution, but that higher resolution simulations will be needed to fully explore the sensitivity of the stellar IMF to the chemical make-up of the gas.

4 DISCUSSION

Our simulations demonstrate that once a dense, gravitationally unstable cloud of gas has formed in the ISM, molecular cooling is not required in order to convert this gas into stars. In the absence of molecules, the cooling provided by the C\(^+\) fine-structure line at \(\nu < 2 \times 10^{16}\) cm\(^{-1}\) and by dust at \(\nu > 2 \times 10^{16}\) cm\(^{-1}\) are sufficient to allow stars to form. However, we cannot conclude solely from this that molecular gas is an inessential component of the star formation process. A skeptic could well argue that molecular cooling may be required in order to form the dense cloud of gas that we take as the initial conditions for our simulations, an assertion that our current results can obviously do nothing to address. Fortunately, the issue of the assembly of cold, dense clouds of gas from the warm, neutral ISM has already been investigated by a number of authors (see e.g. Koyama & Inutsuka 2002; Audit & Hennebelle 2005; Vázquez-Semadeni et al. 2007; Heitsch et al. 2008; Heitsch & Hartmann 2008; Banerjee et al. 2009).

These studies typically make use of a set-up that involves converging flows of warm atomic gas, with an initial temperature and density corresponding to the warm neutral medium (WNM). The thermal models adopted vary somewhat in complexity, from a simple two-parameter cooling function introduced by Koyama & Inutsuka (2002) and used in a number of later works (e.g. Vázquez-Semadeni et al. 2007; Banerjee et al. 2009), to the more detailed treatment used in e.g. Audit & Hennebelle (2005) that accounts explicitly for photoelectric heating from dust and fine-structure cooling from C\(^+\) and O. However, one common feature is that these models do not account for cooling coming from H\(_2\) or CO. Indeed, they typically do not include any non-equilibrium chemistry. Despite this, these models readily produce cold, dense clouds of gas in the region where the converging flows intersect. These cold clouds
are produced initially by a thermal instability acting in the WNM that relies primarily on C\(^+\) cooling. The clouds can then collide and agglomerate, forming gravitationally bound structures.

The typical densities and masses of the cold clouds formed in these converging flow studies span a wide range of values, depending on the size of the simulation volume and the effective resolution of the simulation. Large-scale converging flow simulations, such as that performed by Banerjee et al. (2009), have shown themselves capable of producing cold clouds with properties similar to those we take as our initial conditions (i.e. a mean density of a few hundred cm\(^{-3}\) and a cold gas mass of 10\(^4\) M\(_\odot\)) even though these simulations do not include molecular cooling. Models of cloud formation on the scale of the Galactic disc also appear to have no difficulty in producing large cold gas clouds without needing to invoke molecular cooling (see e.g. Tasker & Tan 2009). Taken together with our results, this implies that molecular gas is not necessary for star formation: it is possible to form both cold, dense clouds, and also stars within these clouds, without needing to rely on molecular cooling.

If molecular gas is not a prerequisite for star formation, then why is it that we find such a good observational correlation between the surface density of molecular gas and the star formation rate surface density? An obvious explanation is that both the presence of molecular gas and the propensity of a gas cloud to form stars are correlated with some third factor, such as the column density of the cloud. An argument along these lines was given by Schaye (2004), who pointed out that in regions of the Galactic disc with gas surface densities of less than 10 M\(_\odot\) pc\(^{-2}\), ionization and heating of the gas by the extragalactic radiation field prevent the formation of a cold, neutral phase. The transition from the WNM to the cold neutral medium is associated with a dramatic decrease in the Jeans mass of the gas, and Schaye (2004) argues that this is the trigger for star formation. The transition from atomic to molecular gas coincidentally occurs at roughly the same surface density (see e.g. Browning, Tumlinson & Shull 2003; Krumholz et al. 2009), and so the result is a correlation between the presence of molecular gas and the formation of stars.

The Schaye (2004) model assumes that all cold clouds form stars, but as we have seen in this paper, this is probably an oversimplification. In a more recent paper, Krumholz et al. (2011) look in more detail at the chemistry and thermodynamics of cold clouds in the ISM. They use simple 1D cloud models that assume chemical and thermal equilibrium to explore a range of different cloud densities and visual extinctions, and show that in these models, the transition from atomic to molecular hydrogen is well correlated with a further sharp drop in the equilibrium gas temperature. This correlation is not a result of H\(_2\) cooling. Rather, it occurs because the conditions required in order to attain a low gas temperature – high densities to boost C\(^+\) cooling, and efficient dust shielding to suppress photoelectric heating – are similar to those required to produce a high equilibrium H\(_2\) fraction. They then argue that star formation is strongly correlated with regions of cold gas, owing to the T\(^{3/2}\) temperature dependence of the Bonnor–Ebert mass scale, which makes gravitational fragmentation much easier to bring about in cold gas than in warm gas. In both of these models, the correlation between H\(_2\) and star formation comes about because the H\(_2\) traces (but does not cause) the regions where the thermal pressure is low enough to allow stars to form.

The results from our present study provide strong support for this picture. They show that H\(_2\) cooling plays an insignificant role in determining the cloud temperature, that the differences between the temperatures of clouds cooled solely by C\(^+\) or by a mix of C\(^+\) and CO are very similar, and that the key factor enabling star formation within the clouds is the shielding of the ISRF by dust. In the absence of this shielding, the temperature of the gas remains high, star formation is strongly suppressed and the H\(_2\) abundance is very small.

5 CONCLUSIONS

In this study, we have investigated whether or not the formation of molecular gas is a prerequisite for star formation. We have performed simulations using different chemical models: one in which the gas is assumed to remain atomic throughout, a second in which H\(_2\) formation is included, but CO formation is not, and a third which follows both H\(_2\) and CO formation. We find only minor differences in the nature and rate of star formation in these simulations. In contrast, disabling the effects of dust shielding has a very strong effect: the gas temperature does not fall much below a few 100 K and the formation of stars is strongly suppressed.

We infer from these results that the observational correlation between H\(_2\) and star formation is not a causal relationship: H\(_2\) and CO are not required for star formation, and the fact that we find a good correlation between the H\(_2\) surface density and the star formation rate surface density simply reflects the fact that both are correlated with some third factor. Our results suggest that the key factor is the ability of the clouds to shield themselves effectively against the ISRF: clouds that are too diffuse to shield themselves do not cool and hence form few, if any stars. Since effective shielding of the UV background is also required in order to form large abundances of H\(_2\) or CO (Glover et al. 2010; Glover & Mac Low 2011), this naturally leads to a correlation between molecular gas and star formation without the necessity for a direct causal link between them.

Our current results do not allow us to establish whether the column density of dust required to provide effective shielding is independent of the cloud properties, or a function of the mean density of the gas; this will be addressed in future work.

Finally, it is interesting to speculate about the possible observational consequences of this result. One possible way of testing this model would be to look for regions in which ongoing star formation is not accompanied by significant amounts of molecular gas. If molecular gas is required for star formation, then it would be very difficult to explain the existence of such regions, whereas they are easily accommodated within our model. Unfortunately, such regions are likely to be rare, since they require the molecular gas fraction to be far out of equilibrium, and as our models show, high molecular fractions can be reached within a single free-fall given typical Galactic conditions. If our results hold at lower metallicities (which is a reasonable assumption, but one which must be tested by future simulations), then one promising place to look for such regions would be within low-metallicity star-forming dwarf galaxies such as IZw 18 or DDO 154, since in these systems the characteristic chemical time-scales will be much longer. Indeed, efforts to date to detect CO within these galaxies have been unsuccessful (Leroy et al. 2007; Komugi et al. 2011), although whether this is due to a general deficit of molecular gas or simply a low CO-to-H\(_2\) ratio remains unclear.

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