Development of multi diagonal based OCDMA system for free space optical communication system

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Abstract
The performance of FSO communication link is subject to numerous atmospheric factors in wireless communication like fog, rainfall, and haze which leads to deteriorate the performance of a system in term of BER and power at the receiver side. Due to numerous advantages of OCDMA over other access techniques, it allows various users to access a channel simultaneously without intervention with the other user. It has the ability to provide security, large number of users, privacy, reduce interference from multiple users and operate asynchronously. So, in this paper, Multi-Diagonal codes along with the fiber brags grating filters for Spectral amplitude coded OCDMA technique is developed for FSO system and performance analysis is performed in terms of BER and received power.

Keywords Free space optics (FSO) · Optical code division multiple access (OCDMA) · Multi access interference (MAI) · Multi diagonal (MD) code · Zero cross correlation (ZCC)

1 Introduction
Optical communication provides the solution towards increasing spectrum requirement. With the help of different multiple access techniques, the problem of huge spectrum requirement can be solved. These techniques provide sharing and access of spectrum efficiently. Generally, three access techniques have been used in optical communication i.e. Optical Time Division Multiple Access (OTDMA) (Yeh et al. 2019), Wavelength Division Multiple Access (WDMA) (Kumari et al. 2019), and Optical Code Division Multiple access (OCDMA). In OCDMA, for every user a unique code is assigned in an optical communication network. The major advantages (Islam et al. 2019) of OCDMA are that it can work
asynchronously, can support larger number of users, flexible to add users in the network, provides security against eavesdropping, no need for controlling the existing network, and it does not require any scheduling. So, OCDMA is considered as the most promising technology. The performance of OCDMA network degrades due to various noises such as dark current noise, thermal noise, and multiple access interference (MAI) generated from multiple users. To minimize the effect of MAI (Zouine et al. 2019), different code sequence are assigned to various users. The code sequence designed using Spectral Amplitude Coding–OCDMA (SAC-OCDMA), provides better solution which helps in reducing the effect of MAI. Various codes have been developed for SAC-OCDMA. Amongst these codes optical orthogonal codes (OOCs) offers better cross and auto- correlation properties as compare to other codes.

FSO communication captured great attention due to its high-speed line of sight communication, and utilizes a light beam to transmit information through atmospheric medium instead of optical fiber. Since it is an unguided medium, so due to its numerous advantages, it can be utilized in various telecommunication applications. It is very challenging to communicate at those places where laying down of fiber is a difficult. So FSO appears to be the best alternative for communication. In wireless communication, FSO have numerous advantages like, license-free communication, high data rate. But weather conditions plays a very crucial role in FSO communication. Due to bad weather the performance of the optical link gets affected (Kundu et al. 2017). Line of sight communication is affected by Fog and Rainfall condition, due to the decrease in visibility. For supporting many users simultaneously in shared media, OCDMA has been recognized as one of the most important technologies, and in some cases transmission capacity of an optical fiber can be increased by assigning unique code. OCDMA systems provides good data rate for small distances like within a city.

In literature, different orthogonal codes are available for implementing OCDMA technique (Li et al. 2019). Such as in (Kaur et al. 2015) diagonal double weight (DDW), in (Rani et al. 2018) modified double weight (MDW) code, in (Mostafa et al. 2017) modified quadratic congruence (MQC) codes and in (Fayadh et al. 2018) multi-diagonal (MD) codes are implemented. MD code provides zero cross correlation amongst various users placed in the optical network, which supresses the effect of MAI due to other users, and offers flexibility in selecting the code weight for simultaneous users.

In this work, the Fiber Bragg Grating (FBG) dispersion compensation module is used to optimize the existing MD coded FSO system to achieve a better performance in terms of data rate. Furthermore, we compared the system performance under different weather conditions and analyse the system behaviour. The paper is organised as follow: we present in Sect. 2 different attenuations due to weather conditions. In Sect. 3, we present the MD code for our system. Section 4 is dedicated to system design & simulation setup. Finally results in Sect. 5 followed by the conclusion.

2 Specific Attenuation of rain & fog

Since FSO is a line of sight communication, so the performance depends on various environmental factors like rainfall, fog and snow. BER and received signal power gets affected due to attenuation present in the FSO medium. Amongst various environmental factor, atmospheric attenuation plays a very important role. Generally, attenuation due to fog dominates in atmospheric medium due to particle size comparable with the FSO
system wavelength used. Scattering, absorption, fading and reflection can hinder or alter the optical characteristics. Environmental conditions can be predicted with the help of visibility. In order to compute the optical parameters from atmospheric parameters, several models describe the relationship between attenuation and visibility range are given in (Kim et al. 2001). Specific attenuation in dB/km is used to characterize the medium, and it can be calculated using Eq. (1):

\[ \beta(\lambda) = \frac{1}{D} \log \left( \frac{P_E}{P_D} \right) = \frac{1}{D} 10 \log \left( e^{\gamma(D)} \right) \]  

(1)

where \( D(\text{km}) \) is the length of link, \( P_E \) is the emitted optical power, \( P_D \) the optical signal power at distance \( D \), and \( \gamma(D) \) the atmospheric attenuation coefficient. The effect of attenuation due to atmosphere is as follows:

2.1 Fog

Mie scattering theory is used to study the attenuation due to fog. However, detailed information and complex computations and required. A different approach depends on visibility is helpful in predicting atmospheric attenuation constant values. These values can be computed by implementing common empirical model. So, using Eq. (2), attenuation values due to fog can be calculated.

\[ \beta_{\text{fog}}(\lambda) = \frac{3.91}{\text{Vis}} \left( \frac{\lambda}{550} \right)^{-q} \]  

(2)

where \( \lambda(\text{nm}) \) is the wavelength used, \( \text{Vis}(\text{km}) \) stands for visibility distance, and \( q \) is known as size distribution coefficient of scattering, which can be calculated using Kim model (Alnajjar et al. 2017).

\[
q = \begin{cases} 
  1.6 & \text{Vis} > 50 \\
  1.3 & 6 < \text{Vis} < 50 \\
  0.16\text{Vis} + 0.34 & 1 < \text{Vis} < 6 \\
  \text{Vis} - 0.5 & 0.5 < \text{Vis} < 1 \\
  0 & \text{Vis} < 0.5 
\end{cases}
\]  

(3)

Table 1 summarizes different values of specific attenuation in dB/km based on visibility range for various atmospheric weather conditions (Series 2012).

| S.No | Weather type | Visibility Range V (km) | Attenuation dB/km |
|------|--------------|-------------------------|-------------------|
| 1    | Light Fog    | 0.77–1                  | 18.3              |
| 2    | Very Light Fog | 1–1.8                  | 13.8              |
| 3    | Light Mist   | 1.9–2.5                 | 6.6               |

*Table 1 Visibility range and attenuation for fog*
2.2 Rain

Due to small size rain droplets, a scattering is produced which is known as wavelength-independent scattering. Also, there is a linear relationship between specific attenuation and rate of rain. The attenuation due to rate of rainfall $R$ (mm/hr) is given by Eq. (4).

$$\beta_{\text{rain}} = 1.046 R^{0.67}$$

(4)

The specific attenuation for FSO medium under rainfall condition can also be computed using empirical formula given by Eq. (5).

$$\alpha_{\text{rain}} = \frac{2.8}{\text{Vis}}$$

(5)

where Vis is visibility range in km, Table 2 shows the value of specific attenuation under different rainfall condition (ITU-R 2012).

3 MD code

To achieve good performance in terms of BER and received power, codes for OCDMA systems must be unipolar with constant weight and minimum cross-correlation to reduce the effect of MAI. Hence, in (Kumawat et al. 2020) OOCs is a code family which provides low cross-correlation values are discussed. The notation for this type of code is $(L, W, l_a, l_c)$, where $L$ is the length of code sequence, $W$ is the weight, $l_a$ and $l_c$ is the auto-correlation and cross-correlation between any two codes.

In OCDMA networks, in a same time slot multiple simultaneously transmission can be performed through the FSO channel. Codeword must have minimum correlation, so as to avoid the effect of interference to achieve good performance. MD code is implemented in our design due to numerous advantages (Abd et al. 2011):

- It has zero cross-correlation that removes MAI.
- It shows further flexibility to select weight parameters and number of rows of a matrix as compared with other codes such as MQC.
- It is easy to design.
- It can support many users with a high rate of data.
- The code is in a way that overlapping does not occur for spectral characteristic of users.
- For both four-wave mixing and cross-phase modulation nonlinearities, the MD code performs better than the other codes like Multi-weight (MW) and Walsh-Hadamard (WH) codes.

| S.No | Weather type       | Rainfall Rate $R$ (mm/hr) | Visibility Range Vis (km) | Attenuation dB/km |
|------|--------------------|---------------------------|---------------------------|-------------------|
| 1    | Strong Rainfall    | 25                        | 1.9–2                     | 6.9               |
| 2    | Average Rainfall   | 12.5                      | 2.8–4.0                   | 4.6               |
| 3    | Light Rainfall     | 2.5                       | − 10                      | 2                 |

Table 2 Rainfall rate and their visibility range
Moreover, the code length is less in comparison with Khazani–Syed (KS) code so, construction of codes is easy for simultaneous users.

For four users $K = 4$, code weight $W = 2$ the code length $N = 8$, and the corresponding MD code is given by (15).

$$MD = \begin{bmatrix}
1 & 0 & 0 & 0 & 0 & 0 & 1 \\
0 & 1 & 0 & 0 & 0 & 1 & 0 \\
0 & 0 & 1 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1 & 1 & 0 & 0
\end{bmatrix}_{4 \times 8} \quad (6)$$

So, the codeword is achieved in terms of wavelength for individual users as per the coding technique:

$$\text{Codeword} = \begin{cases}
\text{user}1 \Rightarrow \lambda_1, \lambda_8 \\
\text{user}2 \Rightarrow \lambda_2, \lambda_7 \\
\text{user}3 \Rightarrow \lambda_3, \lambda_6 \\
\text{user}4 \Rightarrow \lambda_4, \lambda_5
\end{cases}$$

System Design & Simulation Setup

Two continuous wave lasers are used at the user side with an input power of zero dBm for individual user as per the weight of the code, an ideal $2 \times 1$ multiplexer is used to combine two different wavelengths corresponding to individual user. A user defined bit stream is modulated using NRZ modulation format with the help of MZ modulator. Power combiner or ideal mux is used to combine all the user information, which is further transmitted through the FSO medium. The FSO parameters are specified in Table 3 and at the receiver end, an ideal de-multiplexer, a pair of dispersion compensated FBG is used as a decoder along with the optical adder to combine two different wavelengths, an APD and a low pass Bessel filter is used to recover and reconstruct back in to electrical form. In comparison to typical electric and alternative fibre sensors, FBG provides direct absolute measurement. It has a unique wavelength multiplexing capability for the installation of an optical data bus network. Also, it can make measurements over long ranges with little or no signal loss when coupled with a high-power tunable laser. Analyser is further used to calculate the BER and gives the information regarding eye patterns. Figure 1 shows the completed block diagram of MD codes FSO system. The simulation is performed using OptiSystem15 for 4 users with code weight of 2. Received power is also calculated under FSO system using Eq. (7), where $P_R$ and $P_T$ are received and transmitted power, $d_R$ and $d_f$ is receiver and

| S.No | Parameter                   | Values     |
|------|-----------------------------|------------|
| 1    | Wavelength                  | 1550 nm    |
| 2    | Power                       | −10 dBm    |
| 3    | Number of users             | 4          |
| 4    | Range                       | 0.3 to 2.5 km |
| 5    | Transmitted aperture diameter| 10 cm      |
| 6    | Received aperture diameter  | 25 cm      |
| 7    | Divergence                  | 2 mrad     |
| 8    | Bit Rate                    | 1 Gbps     |
transmitter aperture diameter (m), $\alpha$ is atmospheric attenuation (dB/km), $\theta$ is beam divergence (mrad), and $D$ is the range (km), whereas no atmospheric fading is considered while calculating the optical power.

$$P_R = P_T \frac{d^2}{(d_T + \theta D)^2} 10^{-a D / 10} \quad (7)$$

## 4 Results

A bit stream $0,101,101,110$ is transmitted through FSO and a similar bit pattern is observed on oscilloscope as shown in Fig. 1. Transmitted distance is varied in FSO system and the design is investigated using MD code for different weather conditions. Figure 2 shows that with MD code the signals can transmitted upto 1.2 km with BER of $6.23 \times 10^{-11}$ under strong rainfall. Whereas a significantly high distance of 1.4 km with BER of $3.22 \times 10^{-13}$ is achieved under average rain condition. Under light rainfall, a distance further increased upto 2 km with BER of $7.23 \times 10^{-11}$. Figure 3 shows the variation of received power under different rainfall conditions for first user.

The performance of MD coded OCDMA FSO network under different fog conditions is shown in Fig. 4, under light fog condition, a distance of 700 m is achieved with a significant BER value of $3.20 \times 10^{-13}$. In very light fog, distance of 800 m is achieved with BER of $2.09 \times 10^{-13}$. Figure 5 shows the variation of received power under different fog conditions. As distance increases received power decreases. Atmospheric attenuation, scintillation effect, and Field of View all contribute to the rise in BER. The attenuation dB/km increases as the link distance increases. This path loss lowers received power and
scatters the optical footprint at the receiver side, lowering the optical received signal at the
photo-detector window. Since, SNR and Q-factor are proportional to each other as well as
received optical signals, whereas BER is inversely proportional so, BER increases with
increase in link distance for a fixed value of transmitting power.

MD coded FSO system performs good upto a bit rate of 1.75 Gbps, Fig. 6 shows vari-
ation of different bit rate. Under average rainfall condition a significant distance of 1.3 km
is achieved with a significant BER of $2.46 \times 10^{-12}$. Beam divergence also affect the system
performance, Fig. 7 shows the performance of system under average rainfall condition. The
eye diagram shows that at even for higher values of beam divergence, system performance
is good with BER of $5.34 \times 10^{-12}$.

It can be seen from Fig. 8 that as we increase transmitter aperture diameter, received
power decreases because beamwidth increases which further reduced the transmitted range

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**Fig. 2** BER vs range under different rainfall condition

**Fig. 3** Received Power vs range under different rainfall condition
and received power. Also, in Fig. 9 as receiver aperture diameter increases more optical beam will be collected by the receiver, due to which received power increases.

5 Conclusion

The application of MD coded SAC-OCDMA technique in FSO system have numerous benefits such as security enhancement, flexible channel allocation and at any stage users can be increased. This paper discussed the development of MD OCDMA system & its performance analysis for FSO medium. It illuminated the effect of rainfall and fog attenuation on the system performance along with the beam divergence. In addition, MD
codes are ZCC codes, so it reduces the effect of MAI due to other users and outperforms the codes having low cross-correlation values. System performs well even at higher values of beam divergence. Distance achieved under strong rainfall and light fog conditions are 1.2 km and 700 m.
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