Integrated Modeling of Photosynthesis and Transfer of Energy, Mass and Momentum in the Soil-Plant-Atmosphere Continuum System

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Abstract. Root water uptake is an important component of the terrestrial water balance and a critical factor that influences energy, water vapor, and carbon exchange among soil, vegetation and atmosphere interfaces. However, most of the current vegetation photosynthesis models do not account for root water uptake, which compromises their applications under water stressed conditions. To address this limitation, this study integrates photosynthesis and transfer of energy, mass and momentum in the soil-plant-atmosphere continuum system, via a simplified 1D root growth model and a resistance scheme (from soil, through root zones and plants, to atmosphere). The coupled model was evaluated with field measurement of a maize canopy. The results indicated that the simulation of land surface fluxes was significantly improved due to considering the root water uptake, especially when vegetation is experiencing severe water stress. This finding highlights the importance of enhanced soil heat and moisture transfer, as well as dynamic root distribution, on simulating ecosystem functioning.

Key words: SCOPE model; STEMMUS model; Soil-Plant-Atmosphere Continuum (SPAC) system; Root Water Uptake (RWU); Root system growth

1. Introduction

Root water uptake (RWU) by plants is a critical process controlling water and energy exchanges between the land surface and the atmosphere, as well as the plant growth. The representation of RWU is an essential component of eco-hydrological models that simulate terrestrial water, energy and carbon fluxes (Seneviratne et al., 2010; Wang and Smith, 2004). However, most of these models consider the above-ground processes in much greater detail than below-ground processes, and therefore, they have limited ability represent the dynamic response of plant water uptake to water stress. Compensatory Root
Water Uptake (CRWU) refers to the process by which uptake from sparsely rooted but well-watered parts of the root zone compensates for stress in other parts (Jarvis, 2011). The failure to account for compensatory water uptake and the associated hydraulic lift from deep subsoil (Caldwell et al., 1998; Dawson, 1993) can lead to significant uncertainties in simulating the plant growth and corresponding eco-hydrological processes (Desborough, 1997; Lee et al., 2005; Seneviratne et al., 2010; Teuling et al., 2006; Zeng and Dai, 1998).

Furthermore, the macroscopic RWU model needs to calculate Hydraulic Redistribution (HR) (Caldwell et al., 1998; Espeleta et al., 2004; Amenu and Kumar, 2007; Fu et al. 2016) (Table 1). Ideally, a RWU model is based on the soil-plant-atmosphere continuum concept (SPAC-RWU), and considers the redistribution of soil water with compensatory water uptake as well as the flow of water from soil through the plant to the atmosphere (Guo, 1992).

The spatial (i.e., one dimensional vertical) pattern of RWU is determined by the spatial distribution of the root system, the knowledge of which is essential for predicting the spatial distribution of water contents and water fluxes in soils. The distribution of roots and their growth are sensitive to various physical, chemical, and biological factors, as well as to soil hydraulic properties that influence the availability of water and oxygen for plants (Beaudoin et al., 2009). Many attempts have been made in the past to develop root growth models that account for the influence of various environmental factors such as temperature, aeration, soil water availability, and soil compaction. Existing root growth models ranged from complex, three-dimensional root architecture models (Bingham and Wu, 2011; Leitner et al., 2010; Wu et al., 2005) to much simpler root growth models that are implemented within more complex models such as EPIC (Williams et al., 1989) and DSSAT (Robertson et al., 1993). Most of these models reproduce the measured rooting depth very well, but the distribution of new growth root is based on empirical functions rather than biophysical processes (Camargo and Kemanian, 2016) (Table 1).

Modelling RWU requires representation of above and below ground processes, which is realized via SPAC-RWU. The SPAC-RWU model represents a good compromise between simplicity (i.e., a small number of tuning parameters) and the ability to capture non-linear responses of RWU (and subsequently the ecosystem functioning) to drought events. Specifically, the SPAC-RWU model calculates the CRWU term using the gradient between leaf water potential and soil water potential of each soil layer. The HR process is an extreme case of CRWU occurring when the transpiration is relatively small and the RWU terms in some soil layers are negative due to leaf water potential was higher than soil water potential. The most important parameters in the SPAC-RWU model include the leaf water potential, stomatal resistance, and the root resistance. Different from other macroscopic models using the root distribution function, the SPAC-RWU model needs explicitly the root length density at each soil layer to calculate the root resistance for each soil layer (Deng et al. 2017). The most practical method for obtaining the root length density is using the root growth model.

To understand the ecosystem functioning under drought stress, the sub-models for below and above ground are therefore needed to be coupled via the afore-mentioned resistance schemes, which control the flow of water from soil to root, root to
plant and plant to atmosphere. Furthermore, the coupling should be realized also via the interface: one sub-model provides the boundary conditions for the other. The below-ground process model simulates the Simultaneous Transfer of Energy, Momentum, and Mass in Unsaturated Soil (i.e., STEMMUS model), the running of which requires land surface energy fluxes and land surface temperature. On the other hand, the required surface boundary state and fluxes can be provided with the above-ground process model, for example, the vegetation photosynthesis model, SCOPE (Soil Canopy Observation, Photochemistry, and Energy Fluxes).

The SCOPE model simulates canopy reflectance and fluorescence spectra in the observation directions, as well as photosynthesis, and evapotranspiration as functions of leaf optical properties, canopy structure, and weather variables (Van der Tol et al. 2009). SCOPE model provides a valuable means to study the link between vegetation appearance and ecosystem functioning, however, it does not consider the water budget in soil and vegetation. As such, there is no explicit parametrization of the effects of soil moisture variations on the photosynthetic or stomatal parameters. Consequently, soil moisture effects are only ‘visible’ in SCOPE model if the lack of soil moisture affects the optical or thermal appearance of the vegetation (i.e., during water stress period). The lack of such link between soil moisture availability and vegetation appearance compromises the capacity of SCOPE for predicting/simulating drought events.

The change of vegetation optical appearance as a result of soil moisture variations can only explain partially the soil moisture effect on ecosystem functioning (Bayat et al., 2018), which leads to considerably biased estimations of GPP (Gross Primary Productivity) and ET (Evapotranspiration) in water limited conditions. This presents a challenge for using SCOPE for ecosystems in arid and semi-arid areas, where water availability is the primary limiting factor for vegetation functioning. This challenge becomes even more relevant considering that soil moisture deficit or “ecological drought” is expected to increase in both frequency and severity at nearly all ecosystems around the world (Zhou et al., 2013). Bayat et al. (2019) incorporated the SPAC model into SCOPE to address water stress conditions at a grassland site, but the coupled model neglected the dynamic development of root distribution at different soil layers and soil moisture serves only as a model input coming from measurements.

In this study, the modelling of above-ground radiation, energy fluxes in the vegetation layer (i.e., SCOPE) will be fully coupled with the soil heat and mass transfer model - STEMMUS (Simultaneous Transfer of Energy, Mass and Momentum in Unsaturated Soil). The root growth model and the corresponding resistance scheme (from soil, through root zones and plants, to atmosphere) will be integrated for the dynamic modeling of water stress and root system, enabling the seamless modelling of soil-water-plant-energy interactions. The next section of methodology describes the coupling scheme between SCOPE and STEMMUS models, followed by the section of results verifying the coupled SCOPE_STEMMUS model at a maize agroecosystem located in a semi-arid region. The discussion session explores and reveals the dynamic responses of leaf water potential and root length density to water stress. The summary of this study and the further challenges are addressed in the section of conclusions.
Table 1. Comparison of LSMs and crop models in terms of sink term calculation of soil water balance.

| Model   | Sink term calculation of soil water balance | Root water uptake process               |
|---------|--------------------------------------------|----------------------------------------|
| **LSMs** |                                            |                                        |
| CLM4.5  | Actual transpiration, root fraction of each soil layer and soil integral soil water availability (Fu et al., 2016) | The Ryel et al. (2002) Function         |
| CLM4.0  | Actual transpiration, root fraction of each soil layer and soil integral soil water availability (Couvreur et al. 2012, Sulis et al., 2019) | HRWU scheme (HRWU model based on hydraulic architecture) |
| CLM4.1 & IBIS2 | Actual transpiration, physical root distribution and the water availability in each layer (Zhang and Wang, 2007) | HRWU scheme (RWU model based on hydraulic architecture) |
| CoLM    | Total transpiration, root fraction in each layer and water stress factor (Zhu et al., 2017) | The Ryel et al. (2002) Function         |
| CABLE   | Maximal efficiency of water uptake by roots and available soil water (Li et al., 2012) | The Ryel et al. (2002) Function         |
| **Crop Models** |                                            |                                        |
| APSIM   | Potential transpiration and soil water supply factor, but implicit root distribution (Kearing et al., 2003) | The Ryel et al. (2002) Function         |
| CropSyst| Difference in water potential between the soil and the leaf, and a total soil-root-shoot conductance (Steckle et al., 2003) | Not considered | Empirical function |
| DSSAT   | Water uptake per unit of root length is computed as an exponential function, and the actual RWU is the minimum of potential transpiration and the maximum capacity of root water uptake (Jones et al., 2003) | Not considered | Empirical function |
| EPIC    | EPIC assumes that water is used preferentially from the top layers, and the potential water supply rate decreases exponentially downward. (Williams et al., 2014) | Not considered | Empirical approach with a compensatory factor |
| SWAP    | Based on the potential transpiration, root fraction and an empiric stress factor relationship (van Dams, 2000) | Not considered | Empirical function |
| WOFOST  | The simplest one, it calculates water uptake as a function of the rooting depth and the water available in that rooting depth without regard to the soil water distribution with depth (Sap et al., 1994) | Not considered | Empirical function |
| SPACSYS | According to empirical root length density distribution in a soil layer, potential transpiration and soil moisture (Wu et al., 2005) | Not considered | Empirical function |
| STICS   | Based on the potential transpiration, root fraction, and soil water distribution, but not process based (Beaudoin et al., 2009) | Not considered | Empirical function |
2. Methodology and Data

2.1. SCOPE and SCOPE_SM Models

SCOPE is a radiative transfer and energy balance model (Van der Tol et al. 2009). It simulates the transfer of optical, thermal and fluorescent radiation of the vegetation canopy and computes ET by using an energy balance routine. SCOPE includes a radiative transfer module for incident solar and sky radiation to calculate the top of canopy outgoing radiation spectrum, net radiation and absorbed photosynthetically active radiation (aPAR), a radiative transfer module for thermal radiation generated internally by soil and vegetation to calculate the top of canopy outgoing thermal radiation and net radiation, an energy balance module for latent heat, sensible heat and soil heat flux, and a radiative module for chlorophyll fluorescence to calculate the top of canopy radiance spectrum of fluorescence at leaf level.

Compared to other radiative transfer models which simplify the radiative transfer processes based on Beer’s Law, SCOPE has well-developed radiative transfer modules which consider the various leaf orientation and the multiple scattering. SCOPE can provide detailed information about net radiation of every leaf within the canopy. Furthermore, SCOPE is based on energy balance and it can simulate soil surface temperature which is a vital boundary condition needed by STEMMUS. In addition, Bayat et al. (2019) developed SCOPE_SM, which was based on SCOPE but considering the effect of soil moisture (as model inputs). Therefore, SCOPE_SM provides the basic framework to couple SCOPE with STEMMUS, however both SCOPE and SCOPE_SM ignored the soil heat and mass transfer processes and the dynamics of root growth. Appendix A.1 lists the main equations of calculating water stress factor within SCOPE (Bayat et al. 2019), the detailed formulation of SCOPE is referred to Van der Tol et al. (2009).

2.2. STEMMUS Model

STEMMUS model is a two-phase mass and heat transfer model with explicit consideration of the coupled liquid, vapor, dry air and heat transfer in unsaturated soil (Zeng et al. 2011a,b; Zeng and Su, 2013; Yu et al. 2018). STEMMUS provides a comprehensive description of water and heat transfer in the unsaturated soil, which can compensate what is currently neglected in SCOPE. The boundary condition needed by STEMMUS includes surface soil temperature, which is the output of SCOPE. In addition, STEMMUS already contained an empirical equation to calculate root water uptake and a simplified root growth module to calculate root fraction profile. As such, STEMMUS has an ideal model structure to be coupled with SCOPE. The main governing equations of STEMMUS are listed in Appendix A.2.

2.3 Dynamic Root Growth and Root Water Uptake

To obtain the root resistance of each soil layer, we incorporated a root growth module to simulate the root length density profile (see Appendix A.3). The simulation of root growth refers to the root growth module in the INRA STICS crop growth
model (Beaudoin et al., 2009), which includes the calculations of root front growth and root length growth. The root front growth is a function of temperature, with the depth of the root front beginning at the sowing depth for sown crops and at an initial value of transplanted crops or perennial crops (Beaudoin et al., 2009). The root length growth is calculated in each soil layer, considering the net assimilation rate and the allocation fraction of net assimilation on root, which is subsequently a function of LAI (leaf area index) and root zone water content (Krinner et al. 2005). The root length density profile is then used to calculate the root resistance to water flow radially across the roots, soil hydraulic resistance, and plant axial resistance to flow from the soil to the leaves (see Appendix A4).

2.4 SCOPE_STEMMUS Coupling

The coupling starts with an initial soil moisture (SM) profile simulated by STEMMUS, which enables the calculation of the water stress factor, a reduction factor of the maximum carboxylation rate ($V_{\text{max}}$). SCOPE is then used calculate net photosynthesis ($A_n$) or gross primary productivity ($GPP$), soil respiration ($R_e$), energy fluxes ($R_n, L_E, H$ and $G$), transpiration ($T$), which is passed to STEMMUS as the root water uptake (RWU). Then, the net ecosystem exchange ($NEE$) can be calculated based on $A_n$ and $R_e$. Surface soil moisture is also used in calculating soil surface resistance and then calculating soil evaporation ($E$). Furthermore, SCOPE can calculate soil surface temperature ($T_{so}$) based on energy balance, which was subsequently used as the top boundary condition of STEMMUS. Based on RWU, STEMMUS calculates the soil moisture in each layer at the end of the time step, and the new soil moisture profile will be the soil moisture at the beginning of next time step, which is repeated as such till the end of simulation period. The time-step of SCOPE_STEMMUS is flexible and the time step used in this study was half hour. Figure 1 shows the coupling scheme of STEMMUS and SCOPE, and Table B.1 shows all the parameter values used in this study.
Figure 1. The coupling scheme of SCOPE_STEMMUS (Yu et al. (2018), Van der Tol et al. (2009)). The explanations of the symbols were the same as in Table B.1.
2.5. Evapotranspiration partitioning

Most studies in partitioning evapotranspiration (ET) use sap flow and micro lysimeter data from in-situ measurements. In this study, we used a simple and practical method to separate evaporation (E) and transpiration (T) proposed by Zhou et al. (2016). Although the behavior of plant stomata is influenced by environmental factors, the potential water use efficiency (\(uWUE_p\), g C hPa\(^{0.5}\)/kg H\(_2\)O) at stomatal scale in the ecosystem with a homogeneous underlying surface is assumed to be nearly constant (Medlyn et al., 2011), and variations of actual \(uWUE\) (g C hPa\(^{0.5}\)/kg H\(_2\)O) can be attributed to the soil evaporation (Zhou et al., 2016). Thus, the method can be used to estimate \(T\) and \(E\) with the quantities of \(ET\), \(uWUE\) and \(uWUE_p\). Another assumption of this method is that the ecosystem \(T\) equal to \(ET\) at some growth stages, so \(uWUE_p\) can be estimated using the upper bound of the ratio of \(GPP \sqrt{VPD}\) to \(ET\) (here \(GPP\) refers to Gross Primary Productivity, and VPD to Vapor Pressure Deficit) (Zhou et al., 2014; Zhou et al., 2016).

Zhou et al. (2016) used the 95\(^{th}\) quantile regression between \(GPP \sqrt{VPD}\) and \(ET\) to estimate \(uWUE_p\), and showed that the 95\(^{th}\) quantile regression for \(uWUE_p\) at flux tower sites was consistent with the \(uWUE\) derived at the leaf scale for different ecosystems. In addition, the variability of seasonal and interannual \(uWUE_p\) was relatively small for a homogeneous canopy. Therefore, the calculations of \(uWUE_p\), \(uWUE\), and \(T\) at the ecosystem scale were as follows:

\[
\begin{align*}
\frac{uWUE_p}{uWUE} &= \frac{GPP \sqrt{VPD}}{ET} \\
\frac{T}{ET} &= \frac{uWUE}{uWUE_p} \\
\end{align*}
\]

The calculation of VPD was based on air temperature and relative humidity data, and the method of gap-filling was the Marginal Distribution Sampling (MDS) method proposed by Reichstein et al. (2005). To calculate \(GPP\), the complete series of net ecosystem exchange (NEE) was partitioned into gross primary production (\(GPP\)) and respiration (\(Re\)) using the method proposed by Reichstein et al. (2005). Finally, \(ET\) was calculated using the latent heat flux and air temperature. Based on \(GPP\), \(ET\) and VPD data, \(T\) can be calculated using the method proposed by Zhou et al. (2016).

Meanwhile, Zhou et al. (2016) discussed the uncertainty of this method, which was mainly caused by: (1) the uncertainty in the partitioning of \(GPP\) (less than 10\%) and \(Re\) based on \(NEE\), which would result in some uncertainty in \(uWUE\); (2) due to the seasonal variation of atmosphere CO\(_2\) concentration, the assumption of \(uWUE_p\) being constant would cause some uncertainty (less than 3\%); (3) the assumption of \(T\) being equal to \(ET\) sometimes during the growing season would cause some uncertainty when vegetation is sparse.

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2.6. Field measurements

To evaluate the performance of SCOPE_STEMMUS in modeling ecohydrological processes, simulation was conducted to compare SCOPE_STEMMUS with SCOPE, SCOPE_SM, and STEMMUS using the observation of fluxes (from 10 June 2017 to 10 October) at the Yangling station (34°17′ N, 108°04′ E, 521 m a.s.l.). Figure 2 illustrates the variations of environmental factors during the maize growing season. As shown in the subfigures, the incoming shortwave radiation ranged from 0 to 1100 W m$^{-2}$ and decreased significantly after Days-After-Sowing (hereafter as DAS) 67. In contrast, the incoming longwave radiation was relatively stable, which was about 400 W m$^{-2}$ during the maize season. The air temperature was relatively high at initial stage and gradually decreased to 5 °C at the late stage. The soil moisture was maintained at a high level except during a drought episode from DAS 15 to 40, and the relative humidity ($RH$) at the late stage was higher than that at the early stage. Two irrigations were carried out on DAS 7 and DAS 41, and the volume of irrigation were 28mm and 64mm, respectively. The leaf area index (LAI) and canopy height (hc) were measured and the peak value was 4.39 m$^2$ m$^{-2}$ and 1.95 m, respectively. Due to the lack of field measurement on root length and soil moisture profile of root zone, we used the simulated results of SCOPE_STEMMUS as the input data of SCOPE_SM to compare the performance of SCOPE_SM with that of SCOPE_STEMMUS. The Eddy Covariance (EC) system was installed on a height-adjustable tripod. The EC system included a three-dimensional sonic anemometer, an open path infrared gas analyser, and a data logger. The detailed descriptions of the instruments can refer to Wang et al. (2020).
2.7. Performance Metrics

The metrics used to evaluate the performance of coupled SCOPE_STEMMUS model include: (1) Root Mean Squared Error \((RMSE)\); (2) coefficient of determination \((R^2)\); and (3) the index of agreement \((d)\). They are calculated as:

\[
RMSE = \sqrt{\frac{\sum_{i=1}^{n}(P_i - O_i)^2}{n}}
\]

\[
R^2 = \frac{\sum_{i=1}^{n}(P_i-O_i)(O_i-\bar{O})^2}{|\bar{O}|}
\]

\[
d = 1 - \frac{\sum_{i=1}^{n}(P_i-O_i)^2}{\sum_{i=1}^{n}(|P_i-\bar{O}|+|O_i-\bar{O}|)^2}
\]

where \(P_i\) is the \(i\)th predicted value, \(O_i\) is the \(i\)th observed value, \(\bar{O}\) is the average of observed values, and \(n\) is the number of samples.

3. Results

3.1. Soil moisture modeling

Comparison of simulated soil moisture \((SM)\) using STEMMUS and SCOPE_STEMMUS and observed ones is presented in Figure 3. The simulated soil moisture at 20 cm depth agreed with the observed values in terms of seasonal pattern. Although slight overestimation occurred at initial and late stages, the dynamics in soil moisture resulted from precipitation or irrigation were well captured. Per the nature of the two models, the coupling of SCOPE with STEMMUS is not expected to improve...
the simulation of soil moisture. However, compared to SCOPE_SM, which used soil moisture measurements as inputs, the coupled SCOPE_STEMMUS improves the simulation of soil moisture dynamics as measured. The deviation between the model simulations and the measurements can be attributed to the following two potential reasons. First, the field observation has errors to a certain extent and the soil moisture sensors may be not well calibrated. Second, in this simulation, we assumed that the soil texture was homogeneous in the vertical direction, whereas the soil properties (e.g. soil bulk density and saturated hydraulic conductivity) may vary with depth in reality, and at different growth stages due to field management practices. For example, the soil bulk density at 40 cm was much higher than that at 20 cm due to the mechanical tillage, especially in the early stage.

![Graphs showing observed and modeled soil moisture with RMSE and d values](https://doi.org/10.5194/gmd-2020-85)

**Figure 3** Comparison of observed and modeled soil moisture at 20 cm (20 cm_SM) and 40 cm depth (40 cm_SM)

3.2. Soil temperature modeling

Simulated soil temperatures ($T_s$) by STEMMUS and SCOPE_STEMMUS at 20 cm and 40 cm depth are shown in Figure 4. In general, both two models can capture the dynamic of soil temperature well. For the simulation of 20 cm temperature, for STEMMUS and SCOPE_STEMMUS, RMSE value was 2.56 °C and 2.58 °C, respectively; d value was 0.92 and 0.92, respectively. For the simulation of 40 cm temperature, RMSE value was 2.06 °C and 2.07 °C, respectively; d value was 0.93 and 0.93, respectively. These results indicate that both models can simulate well soil temperature. However, there also exist some differences between simulation and observation. The largest difference occurred in DAS 40, when the field was irrigated with the flooding irrigation method. This irrigation activity may lead to the boundary condition errors (i.e., for soil surface temperature), which cannot be estimated well enough (e.g., there is no monitoring of water temperature from the irrigation). Meanwhile, the measurement may also have some errors in this period. The fact for the observed soil temperature
at 20 cm and 40 cm to decrease to almost the same level at the same time indicates a potential pathway for preferential flow in the field (see precipitation/irrigation at DAS 40 in Figure 2), and the sensors captured this phenomenon. Nevertheless, the model captures the soil temperature dynamics.

![Graph comparing soil temperature](image)

**Figure 4** Comparison of observed and modeled soil temperature at 20 cm (20 cm\_Ts) and 40 cm depth (40 cm\_Ts).

### 3.3. Energy balance modeling

A comparison of the observed and modeled half-hourly net radiation ($R_n$), sensible heat flux ($H$), latent heat flux ($LE$), and soil heat flux ($G$) using original SCOPE, SCOPE_SM, and SCOPE_STEMMUS were presented in Figure 5. For net radiation and soil heat flux, the simulations of all three models show good agreements with observations. For net radiation, the coefficients of determination ($R^2$) for SCOPE, SCOPE_SM and SCOPE_STEMMUS were 0.99, 1.00, and 0.99, respectively. For soil heat flux, the $R^2$ for SCOPE, SCOPE_SM and SCOPE_STEMMUS were 0.81, 0.79, and 0.80, respectively. For latent heat flux, SCOPE_STEMMUS has a better performance than SCOPE and SCOPE_SM, and the $R^2$ for SCOPE, SCOPE_SM and SCOPE_STEMMUS were 0.82, 0.84, and 0.85, respectively. Furthermore, SCOPE_STEMMUS and SCOPE_SM have a similar performance in the simulation of sensible heat flux, which were better than the performance of SCOPE, the $R^2$ for SCOPE, SCOPE_SM and SCOPE_STEMMUS were 0.70, 0.75, and 0.74, respectively.
Figure 5 Comparison of observed and modeled half-hourly Net radiation (Rn), Latent heat (LE), Sensible heat (H) and soil heat flux (G) by SCOPE, SCOPE_SM and SCOPE_STEMMUS. Subscripts 'm' and 'o' in each plot indicate modeled and observed quantities, respectively. The regression line is indicated in red color with the corresponding regression equation and the $R^2$.

### 3.4. Daily ET, T and E modeling

Simulated daily evapotranspiration (ET) results by SCOPE, SCOPE_SM, STEMMUS and SCOPE_STEMMUS are presented in Figure 6. As shown in the subfigures, the $R^2$ by SCOPE, SCOPE_SM, STEMMUS and SCOPE_STEMMUS were 0.76, 0.82, 0.80 and 0.81, respectively. The RMSE of these four models were 0.84, 0.69, 0.76, and 0.74 mm day$^{-1}$ respectively. For the ET simulation by SCOPE, there were large differences between simulations and observations when the vegetation suffered water stress. For SCOPE_SM, STEMMUS and SCOPE_STEMMUS, because of taking into account the dynamic variation of soil moisture, the simulated ET were closer to observations when the crop experienced water stress. It indicates that SCOPE_STEMMUS, STEMMUS and SCOPE_SM can predict ET with a relatively higher accuracy, especially when the maize was under severe water stress (DAS 30 to 40), and SCOPE_STEMMUS and SCOPE_SM performed similarly well. It is noteworthy that although STEMMUS has considered the effect of soil moisture on ET, the accuracy of STEMMUS was lower than the coupled model (see DAS 40 and DAS 110 in Figure 6). The possible reason is...
the better representation of transpiration in SCOPE model (see Figure 7), which separates the canopy into 60 layers, while STEMMUS only treats the canopy as one layer.

![Figure 6](https://example.com/figure6.png)

**Figure 6** Comparison of modeled and observed daily evapotranspiration (ET) (ETo: observed ET; ETm: modeled ET).

The modeled and observed daily plant transpiration are presented in Figure 7. The $R^2$ value between simulated and observed transpiration were 0.82, 0.86, 0.79, and 0.86, respectively, for SCOPE, SCOPE_SM, STEMMUS and SCOPE_STEMMUS, and RMSE values were 0.60, 0.50, 0.67, and 0.50 mm day$^{-1}$, respectively. Because of ignoring the effect of water stress on transpiration, SCOPE failed to simulate transpiration accurately when the vegetation experiencing water stress. As shown in the figure, SCOPE overestimated transpiration from DAS 20 to DAS40 during the water stress period. Compared with SCOPE, SCOPE_SM, STEMMUS and SCOPE_STEMMUS can capture the reduction of transpiration during the dry period. The performances of SCOPE_STEMMUS and SCOPE_SM were better than that of STEMMUS. The possible reason is the better simulation of the radiative transfer and energy balance at leaf level in the coupled SCOPE_STEMMUS model (as also in SCOPE_SM) and the more accurate root water uptake (compared to that in SCOPE_SM). Nevertheless, SCOPE_STEMMUS slightly underestimated transpiration when the plant is undergoing severe water stress and slightly overestimated it after the crop was irrigated. This is mainly because the actual $V_{c,max}$ was not only influenced by drought but also related to leaf nitrogen content (Xu and Baldocchi, 2003), which was not considered in this study.
Figure 7 Comparison of observed and modeled daily plant transpiration (T) (To: observed T; Tm: modeled T).

Figure 8 shows the modeled and observed half-hourly canopy transpiration. The simulations by SCOPE_STEMMUS and SCOPE_SM are consistent with observation and both are much lower than that by SCOPE. The performances of SCOPE_STEMMUS and SCOPE_SM were consistent with that of SCOPE in the early morning and late afternoon, when the photosynthesis is mainly limited by incident radiation rather than by water stress, intercellular CO₂ concentration and \( V_{\text{cmax}} \).

In the midday, with increasing incident radiation, the photosynthesis was mainly limited by water stress and \( V_{\text{cmax}} \), exactly when the simulations by SCOPE_STEMMUS and SCOPE_SM are much better than that by SCOPE.

Figure 8 Comparison of observed and modeled half-hourly transpiration (T).
As shown in Figure 9 for soil evaporation, the simulation by SCOPE_STEMMUS is closer to observation than those by other models. When using SCOPE to simulate soil evaporation, the soil moisture is set as constant (i.e., 0.25 m$^3$ m$^{-3}$). Therefore, SCOPE generally underestimates soil evaporation when soil moisture is higher than 0.25 and overestimates soil evaporation when it is lower than 0.25. Due to the lack of measurement of soil surface moisture in this study, we use the average soil moisture at root zone simulated by SCOPE_STEMMUS as the input data for SCOPE_SM to calculate soil surface resistance and soil evaporation. Although STEMUS can capture variation of soil evaporation reasonably well, it has higher RMSE value than SCOPE_STEMMUS. This is probably attributed to the comprehensive consideration of radiation transfer in SCOPE, which is lacking in STEMUS. Consequently, the simulation of soil net radiation of the coupled model was more accurate than STEMUS alone. The RMSE value of SCOPE_STEMMUS was 0.60 mm day$^{-1}$, which was lower than those of other three models (i.e. 0.67, 0.65, and 0.64 mm day$^{-1}$ respectively). For SCOPE_STEMMUS, the major differences between simulations and observations occurred in rainy days, which may be caused by errors of soil surface resistance estimation during these periods or the uncertainty of ET partitioning method.

**Figure 9** Comparison of observed and modeled daily soil evaporation (E) (Eo: observed E; Em: modeled E).

### 3.5. Daily NEE modeling

Simulated NEE by SCOPE, SCOPE_SM and SCOPE_STEMMUS and observed NEE were presented in Figure 10. As shown, similar to the simulation of transpiration, SCOPE cannot respond to water stress when simulating NEE. After introducing soil water stress factor in SCOPE_STEMMUS and SCOPE_SM, the simulations of NEE were improved in both models. The consistency between simulated and observed NEE at mid and late stages were higher than those at early and rapidly growth stages. The difference usually occurred when soil moisture increased. The reason is that the simulated NEE...
was calculated by GPP and Re, and Re was not only influenced by soil temperature, but also by soil moisture. However, in this study, we only considered the effect of soil temperature on Re. Many studies evidenced that soil respiration increased with increasing soil moisture, especially when rain or irrigation occurred. Generally, in the summer, soil temperature decreases when raining or irrigating. However, the model only considers the effect of reduced soil temperature on Re, while ignores the positive effect of increasing soil moisture. As such, the simulated soil respiration would decrease with soil temperature dropped. For the late stage, as soil moisture was stable and maintained at a high level, the difference between simulated and observed soil respiration was relatively small. This can also demonstrate that the errors of NEE simulation were mainly caused by the effect of soil moisture on soil respiration.

**Figure 10** Comparison of observed and modeled daily net ecosystem exchange (NEE) (NEEo: observed NEE; NEEm: modeled NEE).

4. Discussion

4.1. Leaf water potential, water stress factor, and root length density

Leaf water potential was a parameter to reflect plant water status. The simulated half-hourly leaf water potential and water stress factor are presented in Figure 11. The leaf water potential was lower when vegetation suffering water stress compared to other periods. The reason is that soil water potential is low due to the low soil moisture and the leaves need to maintain an even lower water potential to suck water from the soil and transfer it to leaves. During mid and late stages, the leaf water potential was sensitive to transpiration demand due to the slowdown of root system growth. As the continuous measurements of the leaf water potential is not available, we compared the simulated leaf water potential to the measurements reported in other literatures.
Many studies have measured midday leaf water potential or dawn leaf water potential. Fan et al. (2015) reported that the leaf water potential of well-watered maize was maintained high between -73 to -88 m and leaf water potential would decrease when soil water content was lower than 80% of field capacity. Martineau et al. (2017) reported the midday leaf water potential of well-watered maize was around -82 m and the midday leaf water potential decreased to -130 m when the maize was suffering water stress. Moreover, O’Toole and Cruz (1980) studied the response of leaf water potential to water stress in rice and concluded that the leaf water potential of rice can be lower than -80 to -120 m when the vegetation is under water stress and the leaves start curling, which was similar to the simulated leaf water potential of maize in this study. Aston and Lawlor (1979) revealed the relationship between transpiration, root water uptake and leaf water potential of maize. These field studies found that leaf water potential is often very low and it reaches valley values at midday. Elfving (1972) developed a water flux model, which was based on SPAC system and evaluated with the orange tree. In his study, the valley value of leaf water potential under non-limiting environmental conditions was about -120 m, which was slightly lower than the simulation in this study.

In this study, the calculation of water stress factor considered the effect of soil moisture and root distribution. The severe water stress was from DAS 30 to DAS 40, and the coupled model performed very well in this period. As the feedback, water stress can also influence root water uptake and root growth, and then influence soil moisture and root dynamic in the next time step. It indicates that the water stress equation used in this study can characterize the reduction of $V_{\text{cmax}}$ reasonably well.

![Figure 11 Simulation of $\psi_{\text{leaf}}$ (leaf water potential, m) and WSF (water stress factor). (The dashed lines represent the range of midday leaf water potential reported in other sites.]}(https://doi.org/10.5194/gmd-2020-85)

Root length density is another vital parameter in root water uptake calculation. As shown in Figure 12, the root length density was high from 10 to 20 cm depth and gradually decrease from 20 cm to 121 cm. Many previous studies have revealed that root length density was influenced by soil moisture, bulk density, tillage, and soil mineral nitrogen (Amato and Ritchie, 2002; Chassot et al., 2001; Schroder et al., 1996). In this study, as we assumed the soil was homogenous, SCOPE_STEMMUS considered the effect of soil moisture but neglected the effect of bulk density and soil mineral nitrogen.
Amato and Ritchie (2002) also found a similar result as this study about the root length density in a maize field. Peng et al. (2012) studied temporal and spatial dynamics in root length density of field-grown maize and found 80% root length density distributed at 0-30 cm depth with peak values from 0.86 to 1.00 cm cm$^{-3}$. Ning et al. (2015) also reported a similar observation of root length density. Chassot et al. (2001) and Qin et al. (2006) reported that root length density can reach 7 cm cm$^{-3}$ at Swiss midlands. Aina and Fapohunda (1986) also found that root length density can reach 2.5 cm cm$^{-3}$ if the maize was well-watered. In Stuttgart, Germany, Wiesler and Horst (1994) observed the root growth and nitrate utilization of maize under field condition. The observed root length density was 2.45-2.80 cm cm$^{-3}$ at 0-30 cm depth which was much higher than in other studies, and decreased to 0.01 cm cm$^{-3}$ at 120-150 cm depth, which was consistent with the observation of Oikeh et al. (1999) at Samaru, Nigeria. Zhuang et al. (2001b) proposed a scaling model to estimate the distribution of root length density of field-grown maize. In their study, measured root length density in Tokyo, Japan decreased from 0.4-0.95 cm cm$^{-3}$ at top soil layer to about 0.1 cm cm$^{-3}$ at the bottom layer. Zhuang et al. (2001a) observed that the root length density of maize was mainly distributed at 0-60 cm depth and the maximum values were about 0.9 cm cm$^{-3}$. These studies indicate that the root length density values were quite variable when it was observed at different sites, nevertheless the simulated root length density was in order of magnitude similar to the observations in previous studies.

![Simulation of root length density (m m$^{-3}$). (The dashed lines represent the measured root length density reported in other sites.)](image)

5. Conclusions

A fundamental understanding of coupled energy, water and carbon flux is vital for obtaining the information of ecohydrological processes and functioning under climate change. The coupled model, SCOPE_STEMMUS, integrating radiative transfer, photochemistry, energy balance, root system dynamic, and soil moisture and soil temperature dynamic, has been proven to be a practical model to simulate detailed land surface processes such as evapotranspiration and NEE.
the coupled model, STEMMUS could provide root zone moisture profile to SCOPE, which was used to calculate water stress factor. On the other hand, SCOPE can provide soil surface temperature to STEMMUS, which was used subsequently as the top boundary condition. The performance of the coupled SCOPE_STEMMUS model in ET partitioning was improved due to the comprehensive radiative transfer scheme in SCOPE. The coupled model has been successfully applied in a maize field.

Through the inter-comparison of SCOPE, SCOPE_SM, STEMMUS, and SCOPE_STEMMUS, we concluded that the coupled STEMMUS_SCOPE can be used to investigate vegetation states under water stress conditions, and to simultaneously understand the dynamics of soil heat and mass transfer, as well as the root growth. However, there are some needs for further studies to enhance the capacity of STEMMUS_SCOPE in understanding ecosystem functioning. First of all, the estimation of soil boundary condition especially during the irrigation period, which has significant influence on the simulation of soil temperature, needs further improvement. Second, the soil respiration model used in SCOPE, which neglected currently the effect of soil moisture, should be upgraded in the coupled model. Nevertheless, the SCOPE_STEMMUS may be used as an observation operator to assimilate remote sensing data such as solar-induced chlorophyll fluorescence, to improve the estimation of water and carbon fluxes. SCOPE_STEMMUS could also be used to investigate regional or global land surface processes, especially in arid and semi-arid regions, due to its sensitivity to water stress conditions.

Code and data availability. The development and validation of SCOPE_STEMMUS in this paper were conducted in MATLAB R2016a. The exact version of the model used to produce the results used in this paper is archived on Zenodo (Wang et al., 2020). The original source of the SCOPE model and STEMMUS model was obtained from Van der Tol et al. (2009) and Zeng et al. (2011a, b), respectively. The tower-based eddy-covariance measurements used for model validation were obtained from the authors in Yangling, China (Wang et al., 2019).

Author contributions. YW, YZ, LY, PY, CV, ZS and HC designed the study, Developed the code, conducted the analysis, and wrote the manuscript with YW and HC collected and shared their eddy-covariance measurements for the purpose of model validation. All authors gave comments and contributed to the final version of the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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Appendix A

A.1. Water Stress Factor in SCOPE

The C4 Photosynthesis is calculated in the SCOPE model as the minimum of three processes (Farquhar et al., 1980); (1) carboxylation rate limited by Ribulose biphosphate-carboxylase-oxygenase activity (known as Rubisco (enzyme)-limited, $V_c$, described in Eq. (A1)); (2) carboxylation rate limited by Ribulose 1–5 bisphosphate regeneration rate (known as RuBP (electron transport/light)-limited), $V_e$, described in Eq. (A2); (3) At low CO$_2$ concentrations, carboxylation rate limited by intercellular CO$_2$ partial pressure ($p_i$), $V_s$, described in Eq. (A3).

$$V_c = V_{cmax} \cdot WSF$$  \hspace{1cm} (A1)

$$V_e = \frac{\frac{b\pm\sqrt{b^2-4ac}}{2a}}{J}$$  \hspace{1cm} (A2)

$$V_s = \frac{p_i(k_p - \frac{J}{p_i})}{P}$$  \hspace{1cm} (A3)

$$A_n = min(V_c, V_e, V_s)$$  \hspace{1cm} (A4)

$$C_i = C_a(1 - \frac{1}{m_{RH}})$$  \hspace{1cm} (A5)

where $V_{cmax}$ is the maximum carboxylation rate ($\mu$mol m$^{-2}$ s$^{-1}$), $p_i$ is the intercellular CO$_2$ partial pressure (Pa), $k_p$ is a pseudo-first-order rate constant for PEP carboxylase with respect to $C_i$, $P$ is the atmospheric pressure; $A_n$ is the net photosynthesis ($\mu$mol m$^{-2}$ s$^{-1}$); WSF is the total water stress factor, $J$ is the electron transport rate ($\mu$mol m$^{-2}$ s$^{-1}$), $C_i$ is the intercellular CO$_2$ concentration ($\mu$mol m$^{-3}$) and $C_a$ is CO$_2$ concentration in the boundary layer ($\mu$mol m$^{-3}$), $m$ is Ball-Berry parameter and RH is relative humidity at the leaf surface (%).

In the study of Bayat et al. (2019), water stress factor was calculated based on the root zone soil moisture content neglecting the distribution of root length. In this study, water stress factor considered both root length distribution and water content in root zone. We use a sigmoid formulation rather than the piecewise function by Bayat et al. (2019). The calculations are as follows:

$$WSF = \sum_{i=1}^{n} RF(i) \cdot WSF(i)$$  \hspace{1cm} (A6)

$$WSF(i) = \frac{1}{1+e^{-100+\theta_{sat}(SM(i)-\frac{\theta_f+\theta_i}{2})}}$$  \hspace{1cm} (A7)

$\theta_i$ is the soil water content at wilting point; $\theta_f$ is the soil water content at field capacity; $\theta_{sat}$ is the saturated soil water content; $WSF(i)$ is the water stress factor at each soil layer; $RF(i)$ is the ratio of root length in soil layer $i$ and its calculation can be found in the appendix A.4; $SM(i)$ is the soil moisture at each soil layer.
A.2. Governing Equations in STEMMUS

A.2.1 Soil water conservation equation

\[
\frac{\partial}{\partial t} (\rho_L \theta_L + \rho_V \theta_V) = -\frac{\partial}{\partial z} (q_{Lh} + q_{LT} + q_{La} + q_{vh} + q_{VT} + q_{Va}) - S = \rho_v \frac{\partial}{\partial z} \left[ K \left( \frac{\partial h}{\partial z} + 1 \right) + D_{TD} \frac{\partial T_s}{\partial z} + \frac{K}{\gamma_w} \frac{\partial \rho_d}{\partial z} \right] + \\
\frac{\partial}{\partial z} \left[ D_{vh} \frac{\partial h}{\partial z} + D_{VT} \frac{\partial T_s}{\partial z} + D_{va} \frac{\partial \rho_g}{\partial z} \right] - S \tag{A8}
\]

where \( \rho_L, \rho_V \) (kg m\(^{-3}\)) are the density of liquid water, water vapor, respectively; \( q_{Lh} \), \( q_{VT} \) (m \(^3\) m\(^{-3}\)) are the volumetric water content (liquid and water vapor, respectively); \( z \) (m) is the vertical space coordinate (positive upwards); \( S \) (cm s\(^{-1}\)) is the sink term for the root water extraction. \( K \) (m s\(^{-1}\)) is hydraulic conductivity; \( h \) (cm) is the pressure head; \( T_s \) (°C) is the soil temperature; and \( P_g \) (Pa) is the mixed pore-air pressure. \( \gamma_w \) (kg m\(^{-2}\) s\(^{-2}\)) is the specific weight of water. \( D_{TD} \) (kg m\(^{-1}\) s\(^{-1}\) °C\(^{-1}\)) is the transport coefficient for adsorbed liquid flow due to temperature gradient; \( D_{vh} \) (kg m\(^{-2}\) s\(^{-1}\)) is the isothermal vapor conductivity; and \( D_{VT} \) (kg m\(^{-1}\) s\(^{-1}\) °C\(^{-1}\)) is the thermal vapor diffusion coefficient. \( D_{va} \) is the advective vapor transfer coefficient (Zeng et al. 2011a,b). \( q_{Lh}, q_{VT}, \) and \( q_{La} \) (kg m\(^{-2}\) s\(^{-1}\)) are the liquid water fluxes driven by the gradient of matric potential, temperature, and air pressure, respectively. \( q_{vh}, q_{VT}, \) and \( q_{va} \) (kg m\(^{-2}\) s\(^{-1}\)) are the water vapor fluxes driven by the gradient of matric potential, temperature, and air pressure, respectively.

A.2.2 Dry air conservation equation

\[
\frac{\partial}{\partial t} [\varepsilon \rho_{da} (S_a + H_s S_L)] = \frac{\partial}{\partial z} \left[ D_e \frac{\partial \rho_{da}}{\partial z} + \rho_{da} \frac{S_a K_a \partial \rho_g}{\rho_a \partial z} - H_c \rho_{da} \frac{q_L}{\rho_L} + (\theta_a D_{vg}) \frac{\partial \rho_{da}}{\partial z} \right] \tag{A9}
\]

where \( \varepsilon \) is the porosity; \( \rho_{da} \) (kg m\(^{-3}\)) is the density of dry air; \( S_a (=1-S_L) \) is the degree of air saturation in the soil; \( H_s (=\theta_s/\varepsilon) \) is the degree of saturation in the soil; \( H_s \) is Henry’s constant; \( D_e \) (m\(^2\) s\(^{-1}\)) is the molecular diffusivity of water vapor in soil; \( K_a \) (m\(^2\)) is the intrinsic air permeability; \( m_a \) (kg m\(^{-2}\) s\(^{-1}\)) is the air viscosity; \( q_L \) (kg m\(^{-2}\) s\(^{-1}\)) is the liquid water flux; \( \theta_a (=\theta_V) \) is the volumetric fraction of dry air in the soil; and \( D_{vg} \) (m\(^2\) s\(^{-1}\)) is the gas phase longitudinal dispersion coefficient (Zeng et al., 2011a,b).

A.2.3 Energy balance equation

\[
\frac{\partial}{\partial t} \left[ \rho_s \theta_s C_s + \rho_L \theta_L C_L + \rho_V \theta_V C_V + \rho_{da} \theta_a C_a \right] (T_s - T_r) + \rho_V \theta_V L_0 - \rho_L W \frac{\partial \theta_L}{\partial t} = \frac{\partial}{\partial z} \left[ \lambda_{eff} \frac{\partial T_s}{\partial z} \right] - \frac{\partial}{\partial z} [q_L C_L (T_s - T_r)] + q_V (L_0 + C_V (T_s - T_r)) + q_a C_a (T_s - T_r) - C_s S (T_s - T_r) \tag{A10}
\]

where \( C_s, C_L, C_V, C_a \) (J kg\(^{-1}\) °C\(^{-1}\)) are the specific heat capacities of solids, liquid, water vapor, and dry air, respectively; \( \rho_s \) (kg m\(^{-3}\)), \( \rho_L \) (kg m\(^{-3}\)), \( \rho_V \) (kg m\(^{-3}\)), and \( \rho_{da} \) (kg m\(^{-3}\)) are the density of solids, liquid water, water vapor, and dry air, respectively; \( \theta_s \) is the volumetric fraction of solids in the soil; \( \theta_L, \theta_V, \) and \( \theta_a \) are the volumetric fraction of liquid water, water vapor, and dry air, respectively; \( T_r \) (°C) is the reference temperature; \( L_0 \) (J kg\(^{-1}\)) is the latent heat of vaporization of
water at temperature $T_r$; $W$ (J kg$^{-1}$) is the differential heat of wetting (the amount of heat released when a small amount of free water is added to the soil matrix); and $\lambda_{eff}$ (W m$^{-1}$°C$^{-1}$) is the effective thermal conductivity of the soil; $q_l$, $q_v$, and $q_a$ (kg m$^{-2}$ s$^{-1}$) are the liquid, vapor water and dry air flux.

A.3. Dynamic Root Growth Modelling

A.3.1. Root front growth

The depth of the root front is firstly initialized either with the sowing depth for sown crops or with an initial value for transplanted crops or perennial crops. The root front growth stops when it reached certain depth of soil or a physical/chemical obstacle preventing root growth, but also stops when the phenological stopping stage has been reached.

$$\Delta Z = \begin{cases} 0 & T_{air} < T_{min} \\ (T_{air} - T_{min}) \ast RGR & T_{min} < T_{air} < T_{max} \\ (T_{max} - T_{min}) \ast RGR & T_{max} < T_{air} \end{cases}$$

(A11)

$$D_Z(t) = D_Z(t-1) + \Delta Z$$

(A12)

where $\Delta Z$ is root front growth at $t$-th time step; $D_Z$ (cm) is root zone depth; $T_{air}$ (°C) is air temperature; $T_{min}$ (°C) is the minimum temperature of root growth; $T_{max}$ (°C) is the maximum temperature of root growth; $RGR$ (cm °C$^{-1}$ day$^{-1}$) is the root growth rate of root front.

A.3.2. Root length growth

In this study, the root distribution in the root zone was realized via simulating the root length growth in each soil layer.

$$\Delta Rl_{tot} = \frac{A_n \ast f_{root}}{R_c \ast R_d \ast \pi \ast r_{root}^2}$$

(A13)

$f_{root}$ is the allocation fraction of net assimilation to root, and $f_{root}$ is assumed as a function of leaf area index (LAI) and root zone water content. $A_n$ is the net assimilation rate (μmol m$^{-2}$ s$^{-1}$). $R_c$ is ratio of carbon to dry organic matter in root, $R_d$ is root length density (m), and $r_{root}$ is radius of the root (0.15*10$^{-3}$ m), and $\Delta Rl_{tot}$ (m m$^{-3}$) is total root length growth.

The limiting factors for allocation are preliminarily computed and they account for root zone soil moisture availability $A_W$, and light availability $A_L$.

$$A_W = max[0.1, \min(1, WSF)]$$

(A14)

where WSF is the averaged soil moisture stress factor in the root zone.

$$A_L = max[0.1, e^{-K_e \ast LAI}]$$

(A15)

where $K_e = 0.15$ is a constant light extinction coefficient.
\[ f_{\text{root}} = \max \left[ r_{\text{min}}, \frac{3A_L}{A_L+2A_W} \right] \]  

(A16)

where \( r_{\text{min}} (= 0.15) \) is the minimum allocation coefficient to fine roots, and \( r_0 \) is a coefficient that indicates the theoretically unstressed allocation to fine roots.

\[ \Delta R_l(i) = \Delta R_l \text{tot} \ast RF(i) \]  

(A17)

where \( RF(i) \) is the allocation fraction of root growth length in layer \( i \), \( \Delta R_l(i) \) is the root growth length in layer \( i \).

\[ R_l^t = R_l^{t-1} + \Delta R_l(i) \]  

(A18)

where \( R_l^t \) and \( R_l^{t-1} \) is the root length of layer \( i \) at time step \( t \) and time step \( t-1 \).

\[ RF(i) = \frac{R_l(i)}{R_{LT}} \]  

(A19)

where \( R_{LT} \) is the total root length in root zone, \( R_l(i) \) is the root length in soil layer \( i \).

### A.4. Root water uptake

The equation to calculate root water uptake and transpiration was as follows:

\[ \sum_{i=1}^{n} \frac{\psi_{s,i} - \psi_l}{r_{s,i} + r_{r,i} + r_{x,i}} = \frac{0.622 \rho_{da}}{P \rho_V} (e_l - e_a) = T \]  

(A20)

where \( \psi_{s,i} \) is soil water potential of layer \( i \) (m), \( \psi_l \) is leaf water potential (m), \( r_{s,i} \) is the soil hydraulic resistance (s \( m^{-1} \)), \( r_{r,i} \) is the root resistance to water flow radially across the roots (s \( m^{-1} \)), and \( r_{x,i} \) is the plant axial resistance to flow from the soil to the leaves (s \( m^{-1} \)). \( e_l \) and \( e_a \) are vapor pressure of leaf and the atmosphere (hPa), respectively, and \( r_a \) and \( r_c \) are aerodynamic resistance and canopy resistance (s \( m^{-1} \)), respectively. \( \rho_{da} \) is the density of dry air (kg \( m^{-3} \)). \( \rho_V \) is the density of water vapor. \( P \) is the atmospheric pressure (Pa). 0.622 is the ratio of the molar mass of water to air.

\( \psi_{s,i} \) is described as a function of soil moisture by Van Genuchten (1980), and the relevant parameters were shown in Table B.1.

The \( r_s \) is calculated by Reid and Huck (1990) as:

\[ r_s = \frac{1}{B K R_D \Delta d} \]  

(A21)

where \( B \) is the root length activity factor, \( K \) is hydraulic conductivity of soil (m s\(^{-1}\)), \( R_D \) is root length density (m \( m^{-3} \)), and \( \Delta d \) is the thickness of the soil layer (m). \( B \) is calculated as:
\[ B = \frac{2\pi}{\ln[(\pi R_D)^{-1/2}/r_{\text{root}}]} \]  \hspace{1cm} (A22)

where \( r_{\text{root}} \) is root radius (m).

The \( r_r \) is estimated as (Reid and Huck, 1990):
\[ r_r = \frac{P_r (\theta_{\text{sat}}/\theta)}{L_v \Delta d} \]  \hspace{1cm} (A23)

where \( P_r \) is root radial resistivity (s m\(^{-1}\)).

The xylem resistance \( r_x \) is estimated by Klepper et al. (1983):
\[ r_x = \frac{P_a Z_{\text{mid}}}{0.5 f L_v} \]  \hspace{1cm} (A24)

where \( P_a \) is root axial resistivity (s m\(^{-1}\)), \( Z_{\text{mid}} \) is the depth of the midpoint of soil layer, and \( f \) is a fraction defined for a specific depth as the number of roots which connect directly to the stem base to total roots crossing a horizontal plane at that depth. We can consider it equal to 0.22 based on Klepper et al. (1983).

The updated root water uptake term is:
\[ S_i = \frac{\psi_{s,i} - \psi_i}{r_{s,i} + r_{r,i} + r_{x,i}} \]  \hspace{1cm} (A25)

Different from other studies which need to calculate the compensatory water uptake and hydraulic redistribution after calculating the standard water uptake of each soil layer, the sink term in this study is calculated by a physically-based model which contain the effect of root resistance and soil hydraulic resistance rather than only considering the root fraction, so the compensary uptake and hydraulic redistribution have been considered when calculating the sink term.
Appendix B.

Table B.1 List of parameters and values used in this study (All the parameters were classified as Air, Canopy, Root and Soil).

| Symbol | Description                                      | Unit       | Value |
|--------|--------------------------------------------------|------------|-------|
| Aerodynamic |                                               |            |       |
| $a\text{PAR}$ | Absorbed photosynthetically active radiation | $\mu\text{mol m}^{-2} \text{s}^{-1}$ |       |
| $e_a$   | Air vapor pressure                              | Pa         |       |
| $e_l$   | Vapor pressure of leaf                           | hPa        |       |
| $P$     | Air pressure                                    | Pa         |       |
| $q_a$   | Humidity above the canopy                        | kg m$^{-3}$|       |
| $q_l$   | Humidity in stomata                              | kg m$^{-3}$|       |
| $r_a$   | Aerodynamic resistance                           | s m$^{-1}$ |       |
| $RH$    | Relative humidity                                | %          |       |
| $R_{li}$| Incoming longwave radiation                      | W m$^{-2}$ |       |
| $R_{in}$| Incoming shortwave radiation                     | W m$^{-2}$ |       |
| $R_n$   | Net radiation                                    | W m$^{-2}$ |       |
| $T_{air}$| Air temperature                                  | $^0\text{C}$|       |
| $u$     | Wind speed                                       | m s$^{-1}$ |       |
| VPD     | Vapor pressure deficit                           | hPa        |       |
| Canopy |                                               |            |       |
| $A_n$  | Net assimilation rate                            | $\mu\text{mol m}^{-2} \text{s}^{-1}$ |       |
| $C_a$  | CO$_2$ concentration in the boundary layer       | $\mu\text{mol m}^{-3}$ |       |
| $C_{ab}$| Leaf chlorophyll content                         | $\mu\text{g cm}^{-2}$ | 80    |
| $C_{ca}$| Leaf Carotenoid content                          | $\mu\text{g cm}^{-2}$ | 20    |
| $C_w$  | Leaf water content                               | g cm$^{-2}$ | 0.009 |
| $C_{dm}$| Leaf dry matter content                          | g cm$^{-2}$ | 0.012 |
| $C_s$  | Senescent material content                       | g cm$^{-2}$ | 0     |
| DAS    | Days after sowing                                | d          |       |
| $ET$   | Evapotranspiration                               | mm day$^{-1}$ |       |
| $GPP$  | Gross primary production                         | g C m$^{-2}$ day$^{-1}$ |       |
| $h_c$  | Canopy height                                    | m          | [0-1.95] |
| $H$    | Sensible heat flux                               | W m$^{-2}$ |       |
| $J$    | Electron transport rate                          | $\mu\text{mol m}^{-2} \text{s}^{-1}$ | 150   |
| Symbol | Description | Unit(s) |
|--------|-------------|---------|
| $K_e$ | Light extinction coefficient | 0.15 |
| $k_p$ | A pseudo-first-order rate constant for PEP carboxylase | |
| $LAI$ | Leaf area index | m$^2$ m$^{-2}$ [0-4.39] |
| $LIDF$ | Leaf inclination distribution function | |
| $LE$ | Latent heat flux | W m$^{-2}$ |
| $LE_c$ | Latent heat flux of canopy | W m$^{-2}$ |
| $m$ | Ball-Berry stomatal conductance parameter | 4 |
| $NEE$ | Net ecosystem exchange | g C m$^{-2}$ day$^{-1}$ |
| $p_i$ | Intercellular CO$_2$ partial pressure | Pa |
| $r_c$ | Canopy resistance | s m$^{-1}$ |
| $Re$ | Ecosystem respiration | g C m$^{-2}$ day$^{-1}$ |
| $T$ | Transpiration | mm day$^{-1}$ |
| $T_c$ | Vegetation temperature | °C |
| $T_{ch}$ | Leaf temperature (shaded leaves) | °C |
| $T_{cu}$ | Leaf temperature (sunlit leaves) | °C |
| $uWUE_p$ | Potential water use efficiency | g C hPa$^{0.5}$/kg H$_2$O |
| $uWUE$ | Water use efficiency | g C hPa$^{0.5}$/kg H$_2$O |
| $V_{cmax}$ | Maximum carboxylation rate | μmol m$^{-2}$ s$^{-1}$ 50 |
| $\psi_l$ | Leaf water potential | m |

**Root**

| Symbol | Description | Unit(s) |
|--------|-------------|---------|
| $A_W$ | Root zone soil moisture availability | |
| $A_L$ | Light availability | |
| $B$ | Root length activity factor | |
| $D_z$ | Root zone depth | cm |
| $f$ | A fraction defined for a specific depth as the number of roots which connect directly to the stem base to total roots crossing a horizontal plane at that depth | 0.22 |
| $fr_{\text{root}}$ | Allocation fraction of net assimilation to root | |
| $P_a$ | Root axial resistivity | s m$^{-3}$ 1*10$^{10}$ |
| $P_r$ | Root radial resistivity | s m$^{-1}$ 0.65*10$^{12}$ |
| $RF(i)$ | The allocation fraction of root growth length in layer $i$ | |
| $Rl_T$ | Total root length in root zone | m |
| $Rl_{i\,t}$ | Root length of layer $i$ at time step $t$ | m |
\( R_{l_{i-1}} \) Root length of layer \( i \) at time step \( t-1 \) m
\( RL(i) \) Root length in soil layer \( i \) m
\( RGR \) Root growth rate of front cm \(^\circ\)C day\(^{-1}\) 0.002
\( RD \) Root length density m m\(^{-3}\)
\( r_{min} \) The minimum allocation coefficient to fine roots 0.15
\( r_0 \) Coefficient of theoretically unstressed allocation to fine roots 0.3
\( r_{root} \) Radius of the root m 0.15*10\(^{-3}\)
\( r_{x,i} \) Plant axial resistance to flow from the soil to the leaves s
\( r_{r,i} \) Resistance to water flow radially across the roots s
\( r_{s,i} \) Soil hydraulic resistance s
\( RC \) Ratio of carbon to dry organic matter in root kg kg\(^{-1}\) 0.488
\( RWU \) Root water uptake m s\(^{-1}\)
\( RF(i) \) The ratio of root length in soil layer \( i \)
\( T_{min} \) Minimum temperature of root growth \(^\circ\)C 10
\( T_{max} \) Maximum temperature of root growth \(^\circ\)C 40
\( \triangle Z \) Root front growth at \( t \)-th step cm
\( \triangle RL_{tot} \) Total root length growth m
\( \triangle RL(i) \) The root growth length in layer \( i \) m

**Soil**

\( C_s \) Specific heat capacities of solids J kg\(^{-1}\) \(^\circ\)C\(^{-1}\)
\( C_L \) Specific heat capacities of liquid J kg\(^{-1}\) \(^\circ\)C\(^{-1}\) 4.186*10\(^{3}\)
\( C_V \) Specific heat capacities of water vapor J kg\(^{-1}\) \(^\circ\)C\(^{-1}\) 1.870*10\(^{3}\)
\( C_a \) Specific heat capacities of dry air J kg\(^{-1}\) \(^\circ\)C\(^{-1}\) 1.255*10\(^{-3}\)
\( D_{TD} \) Transport coefficient for absorbed liquid flow due to temperature gradient kg m\(^{-1}\) s\(^{-1}\) \(^\circ\)C\(^{-1}\)
\( D_{Vh} \) Isothermal vapor conductivity kg m\(^{2}\) s\(^{-1}\)
\( D_{VT} \) Thermal vapor diffusion coefficient kg m\(^{2}\) s\(^{-1}\) \(^\circ\)C\(^{-1}\)
\( D_{Va} \) Advevtive vapor transfer coefficient kg m\(^{2}\) s\(^{-1}\)
\( D_{Vg} \) Gas phase longitudinal dispersion coefficient m\(^{2}\) s\(^{-1}\)
\( D_{e} \) Molecular diffusivity of water vapor in soil m\(^{2}\) s\(^{-1}\)
\( E \) Soil evaporation mm
$G$  Soil heat flux  $W\ m^{-2}$

$h$  Soil matric potential  $cm$

$H_c$  Henry’s constant  0.02

$K$  Hydraulic conductivity  $m\ s^{-1}$

$K_s$  Intrinsic air permeability  $m^2$

$K_{ws}$  Saturation hydraulic conductivity  $cm\ day^{-1}$  18

$LE_s$  Latent heat flux of soil  $W\ m^{-2}$

$L_0$  Latent heat of vaporization of water temperature $T_r$  $J\ kg^{-1}$  2497909

$m_a$  Air viscosity  $kg\ m^{-1}\ s^{-1}$  $1.846\times10^{-5}$

$n$  Soil-dependent parameter  1.41

$P_s$  Mixed pore-air pressure  $Pa$

$q_L$  Liquid water flux  $kg\ m^{-2}\ s^{-1}$

$q_{lh}$  Liquid water flux driven by the gradient of matric potential  $kg\ m^{-2}\ s^{-1}$

$q_{LT}$  Liquid water flux driven by the gradient of temperature  $kg\ m^{-2}\ s^{-1}$

$q_{La}$  Liquid water flux driven by the gradient of air pressure  $kg\ m^{-2}\ s^{-1}$

$q_v$  Water vapor flux  $kg\ m^{-2}\ s^{-1}$

$q_{vh}$  Water vapor flux driven by the gradient of matric potential  $kg\ m^{-2}\ s^{-1}$

$q_{VT}$  Water vapor flux driven by the gradient of temperature  $kg\ m^{-2}\ s^{-1}$

$q_{Va}$  Water vapor flux driven by the gradient of air pressure  $kg\ m^{-2}\ s^{-1}$

$q_a$  Dry air flux  $kg\ m^{-2}\ s^{-1}$

$S$  Sink term for the root water extraction  $cm\ s^{-1}$

$S_a$  Degree of air saturation in the soil

$S_L$  Degree of saturation in the soil

$SM(i)$  The soil moisture at a specific soil layer  $m^3\ m^{-3}$

$T_s$  Soil temperature  $^0C$

$T_{so}$  Soil surface temperature  $^0C$

$T_r$  Reference temperature  $^0C$  20

$W$  Differential heat of wetting  $J\ kg^{-1}$  $1.001\times10^3$

$WSF$  Total water stress factor

$WSF(i)$  Water stress factor at a specific soil layer

$Z_{mid}$  The depth of the midpoint of soil layer  $m$

$\Delta d$  Thickness of the soil layer  $m$

$\alpha$  Soil-dependent parameter  $m^{-1}$  0.45
| Symbol | Description                                      | Unit         | Value  |
|--------|-------------------------------------------------|--------------|--------|
| \( \theta_{\text{sat}} \) | Saturated water content                        | m³ m⁻³       | 0.42   |
| \( \theta_f \)    | Field capacity                                  | m³ m⁻³       | 0.272  |
| \( \theta_r \)    | Residual water content                         | m³ m⁻³       | 0.0875 |
| \( \theta \)      | Volumetric soil water content                  | m³ m⁻³       |        |
| \( \theta_v \)    | Volumetric vapor content                       | m³ m⁻³       |        |
| \( \theta_s \)    | Volumetric fraction of solids in the soil      | m³ m⁻³       |        |
| \( \theta_a \)    | Volumetric fraction of dry air in the soil     | m³ m⁻³       |        |
| \( \psi_{s,i} \)  | Soil water potential of layer \( i \)          | m            |        |
| \( \psi_{\text{soil}} \) | Soil water potential                           | m            |        |
| \( \lambda_{\text{eff}} \) | Effective thermal conductivity of the soil    | W m⁻¹ °C⁻¹   |        |
| \( \gamma_w \)    | Specific weight of water                       | kg m⁻² s⁻²   |        |
| \( \rho_{\text{da}} \) | Density of dry air                             | kg m⁻³       |        |
| \( \rho_v \)      | Density of vapor                                | kg m⁻³       |        |
| \( \rho_L \)      | Density of liquid water                         | kg m⁻³       | 1      |
| \( \rho_s \)      | Density of solids                               | kg m⁻³       |        |
| \( \varepsilon \)  | Soil porosity                                  | m³ m⁻³       | 0.50   |
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