Synthesis and characterization of nano $\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ for photocatalytic decomposition of $p$-xylene using Box-Behnken design

Sajjad Mafi, Kazem Mahanpoor*

*Department of Chemistry, Arak Branch, Islamic Azad University, Arak, Iran

Received: 13 October 2019, Accepted: 02 November 2019, Published: 23 November 2019

Abstract
$\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ photocatalyst was synthesized by forced hydrolysis and reflux condensation (FHRC) method. In order to fully evaluate the structure, chemical composition and morphology of synthesized composite, various analyses such as XRD, FT-IR, BET, EDX, SEM were applied. In this research, para-xylene was selected as the model substance for photocatalytic reactions to evaluate catalytic ability. To investigate the effect of parameters and select the optimum condition for the understudied process, Box Behnken Design (BBD) due to the Response Surface Methodology (RSM) was performed. For this purpose, catalyst concentration, hydrogen peroxide concentration, initial $p$-Xylene concentration and, pH were selected as important and effective variables. Results showed that the optimized degradation efficiency was close to 96.68% within 90 min. Based on the results, it was found that the initial concentration of $p$-Xylene had the greatest effect on the removal of contamination. Moreover, it was determined that the photocatalytic efficiency of the synthesized composite is more favorable than the non-supported $\alpha$-Fe$_2$O$_3$.

Keywords: Photocatalyst; FHRC; Mn$_2$P$_2$O$_7$; $p$-Xylene; Box Behnken design.

Introduction
Increasing the amount of volatile organic compounds (VOCs) has become one of the environmental challenges of today. These compounds have harmful effects, such as damage to the ozone layer and the greenhouse effect [1]. VOCs usually emit from different sources such as printing and coating facilities, foundries, chemical industries, electronics, and paint manufacturing. Xylene is an example of this type of compound. It is a clear, colorless and hydrophobic liquid that has a characteristic smell [2]. This compound is usually applied as a solvent in printing, rubber, synthetic fiber, plastic, insecticide, pesticides and leather industries, and as a cleaner and a paint thinner [3]. Xylene is toxic to the liver, kidneys and the central nervous system when it comes into contact with skin or breathing system [4]. Isomers of xylene can be found in the list of hazardous and toxic atmospheric contaminants under...
Among different methods such as incineration, condensation, adsorption, absorption, ozonation and membrane separation technologies, photocatalysis is a very advanced strategy to degrade VOCs, due to its unique properties, including good efficiency, high mineralization, non-toxicity and easy accessibility [5]. In chemistry, photocatalysis is the acceleration of a photoreaction in the presence of a catalyst. In catalyzed photolysis, light is absorbed by an adsorbed substrate. In photogenerated catalysis, the photocatalytic activity (PCA) depends on the ability of the catalyst to create electron-hole pairs, which generate free radicals (e.g. hydroxyl radicals: •OH) able to undergo secondary reactions such as decomposition of pollutants [6].

Recently, much attention has been directed toward the production of nanoparticles [7], especially magnetic nanoparticles [8]. Iron (III) oxide or ferric oxide is the inorganic compound with the formula Fe₂O₃. It has many applications in the field of pigment production, catalysis, and medicine [9]. It is one of the three main oxides of iron. Fe₂O₃ has four polymorphs of α-, β-, ε-, and γ-Fe₂O₃. Among them, due to its cost-effectiveness, stability, eco-friendly and visible light harvesting ability, hematite (α-Fe₂O₃) as an n-type semiconductor with narrow band gap (2.0-2.2 eV), is widely used for photocatalytic degradation of pollutants. However, the point that should be noted is that these photocatalytic particles accumulate without any support, which decreases surface area and ultimately reduces photocatalytic activity.

Pyrophosphate (PPi), as an inorganic compound, is a diphosphate tetra-anion (P₂O₇⁴⁻, [O₂-P-O-PO₃]⁴⁻ ) which has attracted a lot of attention due to its versatile coordination modes, low toxicity and biocompatibility [10]. Among them, manganese pyrophosphate, Mn₂P₂O₇, has been found to have an effective catalytic effect on the oxidative dehydrogenation of hydrocarbons and has also interesting magnetic properties at different temperatures, and it has been recommended as a standard material for magnetic susceptibility measurements [11]. However, here the manganese pyrophosphate was used to immobilize α-Fe₂O₃ nanoparticle.

In the present work, the composite of α-Fe₂O₃ nanoparticle and manganese pyrophosphate were synthesized using the Forced Hydrolysis and Reflux Condensation (FHRC) method. In order to make a comprehensive evaluation, the synthesized structure was investigated using characterization methods such as XRD, FTIR, EDAX, BET, and SEM. The synthesis of this compound results in the improvement of photocatalytic properties as well as the recyclability of the catalytic system. In order to investigate the different parameters of the photocatalytic process, i.e. the initial concentration of p-Xylene, the initial concentration of H₂O₂, concentration of catalyst and pH, Box-Behnken design (BBD) due to the Response Surface Methodology (RSM) was performed. A response surface methodology (RSM) might be applied to mapping a design space using a relatively small number of experiments. RSM provided an estimate of the response values for any possible combination of variables by modifying the number of involved factors in parallel.

The design method of response surface methodology is as follows [12]:

1. Designing a series of experiments for appropriate and
dependable measurement of the response of interest
2. Expanding a mathematical model of the second-order response surface with the best fittings
3. Exploring the optimal set of experimental parameters that generate a maximum or minimum value of the response
4. Demonstrating the direct and interactive effects of process parameters using two and three-dimensional graphs

Generally, a second-order model is used in response surface methodology [13].

\[ y = \beta_0 + \sum_{i=1}^{k} \beta_i x_i + \sum_{i=1}^{k} \sum_{j=1}^{k-i} \beta_{ij} x_i x_j + \varepsilon \]  

(1)

In the aforementioned equation \( x_1, x_2, \ldots, x_k \) are the input factors which influence the response \( y; \beta_0, \beta_{ii} (i = 1, 2, \ldots, k), \beta_{ij} (i = 1, 2, \ldots, k; j = 1, 2, \ldots, k) \) are unknown parameters and \( \varepsilon \) is a random error. The \( \beta \) coefficients, which must be quantified in the second-order model, are obtained by the least square method. Generally, Eq. 1 can be written in matrix form as follows:

\[ y = bX + \varepsilon \]  

(2)

where \( y \) can be defined to be a matrix of measured values and \( X \) is a matrix of independent variables. In general, the matrixes \( b \) and \( \varepsilon \) consist of coefficients and errors, respectively.

**Experimental**

**Materials**

Iron (III) chloride hexahydrate was purchased from Daejung Company (Korea). Urea, ethylene glycol, EtOH (96%) and phosphorus pentasulfide (P$_2$S$_5$), manganese powder, and p-Xylene were purchased from Merck (Germany). Hydrogen peroxide (30%) was purchased from Chem Lab Company (Belgium).

**Synthesis of manganese pyrophosphate (Mn$_2$P$_2$O$_7$)**

Manganese pyrophosphate was synthesized in solvothermal condition and through the reaction between Mn metal powder and P$_2$S$_5$ species. Initially, 0.002 mol of Mn and 0.002 mol of P$_2$S$_5$ precursors were mixed with 30 mL of ethylene glycol in a Teflon-lined stainless steel autoclave. The autoclave was completely sealed and placed at 190 °C for 24 h. After this period, the autoclave was allowed to cool down to room temperature. The resultant was centrifuged to collect carefully from the reaction medium and then the separated precipitate was rinsed with distilled water and ethanol. After the synthesis of Mn$_2$P$_2$O$_7$, in order to evaluate its properties and prepare the considered nano photocatalyst, manganese pyrophosphate was dried-up at 60 °C in a vacuum oven.

In the synthesis step of the pyrophosphate species, ethylene glycol also plays a reactant role in addition to the solvent. The reactions carried out during the synthesis of manganese pyrophosphates are as follows:

\[ \text{HOCH}_2\text{CH}_2\text{OH} \rightarrow \text{CH}_3\text{CHO} + \text{H}_2\text{O} \]  

(3)

\[ \text{P}_2\text{S}_5 + 8\text{H}_2\text{O} \rightarrow 5\text{H}_2\text{S} + 2\text{H}_3\text{PO}_4 \]  

(4)

\[ 2\text{Mn} + 2\text{H}_3\text{PO}_4 \rightarrow \text{Mn}_2\text{P}_2\text{O}_7 + \text{H}_2\text{O} + 2\text{H}_2 \]  

(5)

The overall reaction will be as follows:

\[ 2\text{Mn} + \text{P}_2\text{S}_5 + 7\text{HOCH}_2\text{CH}_2\text{OH} \rightarrow \text{Mn}_2\text{P}_2\text{O}_7 + 7\text{CH}_3\text{CHO} + 5\text{H}_2\text{S} + 2\text{H}_2 \]  

(6)

**Synthesis of \( \alpha-\text{Fe}_2\text{O}_3/\text{Mn}_2\text{P}_2\text{O}_7 \) nano photocatalyst using FHRC method**
Initially, 50 mL iron (III) chloride hexahydrate with a concentration of 0.25 M was poured into a beaker. In the next step, 4 g Mn$_2$P$_2$O$_7$ was added slowly under vigorous agitation. The resulting mixture was stirred for 4-5 h. In the next step, stirring was stopped to allow solids to be precipitated. The separated solid transferred into a 50 mL flask. After stirring the solution in the flask, 50 mL urea 1 M was gradually added to it. The mixture was maintained at 90 °C for 12 h under reflux condition. The obtained precipitate after separation was washed with a 1:1 solution of ethanol to deionized water to remove unreacted ions. The resultant was maintained at room temperature for 2 h and then dried at 80 °C for 2 h. Finally, the calcination process was carried out at 300 °C for 1 h.

**General procedure for photocatalytic degradation of p-xylene**

The overall schematic of the used photocatalytic reactor is shown in Figure 1. For each experiment, 250 mL of p-xylene was introduced into the reactor. The amount of p-xylene removal as the pollutant species is determined using the following equation:

$$X\% = \frac{COD_0-COD_t}{COD_0} \times 100$$  \hspace{1cm} (7)

where COD$_0$ was the p-xylene concentration at time zero and COD$_t$ was the corresponding amount at time t.

**Characterization methods**

Powder X-ray diffraction (PXRD) patterns of the synthesized samples were recorded on a D5000 Siemens model diffractometer using Cu Kα radiation (40 kV and 40 mA). FT-IR spectra were recorded on a Thermo Avatar spectrometer using the KBr pellet technique in order to identify the solid powder samples.

Scanning electron microscopy (SEM) images were obtained on the A Philips XL30 scanning electron microscope system.

In order to identify and determine the amount of existing elements, EDAX measurement was performed using FESEM (TESCAN) apparatus.

The textural property was measured using N$_2$ adsorption-desorption isotherms method on the BET–BJH specific surface area measurement equipment (Micromeretics ASAP 2010 system).
The Chemical Oxygen Demands (COD) were measured by COD Meter and Multiparameter Photometer (Hanna-HI83214).

**Evaluation of photocatalytic performance**

In this research, the design of experiments for the degradation process of p-Xylene was performed using Box-Behnken model. Four independent variables of pH, the concentration of hydrogen peroxide, the concentration of catalyst, and the initial concentration of p-Xylene, in three levels (-1, 0, +1) were tested and shown in Table 1.

**Table 1.** Experimental range and levels of the independent variables

| Independent variables | Range of levels |
|------------------------|-----------------|
|                        | -1  | 0  | +1  |
| pH                     | 5   | 7  | 9   |
| H₂O₂ con. (ppm)        | 0.1 | 0.3| 0.5 |
| Catalyst con. (ppm)    | 60  | 90 | 120 |
| Initial con. of p-Xylene (ppm) | 70  | 100| 130 |

The number of experiments obtained using Box–Behnken model was determined as follows:

$$N = 2K (K-1) + C_0$$

(8)

where N is the number of experiments, K is the number of variables, and C₀ is the number of central point’s [14]. Table 2 shows the details of the performed Box–Behnken design of the experiment.

**Table 2.** Experimental conditions for the photocatalytic process

| Exp. no. | pH | H₂O₂ con. (ppm) | Catalyst con. (ppm) | Initial con. of p-Xylene (ppm) |
|----------|----|-----------------|---------------------|---------------------------------|
| 1        | -1 | -1              | 0                   | 0                               |
| 2        | -1 | -1              | 0                   | 0                               |
| 3        | -1 | 1               | 0                   | 0                               |
| 4        | 1  | 1               | 0                   | 0                               |
| 5        | 0  | 0               | -1                  | -1                              |
| 6        | 0  | 0               | 1                   | -1                              |
| 7        | 0  | 0               | -1                  | 1                               |
| 8        | 0  | 0               | 1                   | 1                               |
| 9        | -1 | 0               | 0                   | -1                              |
| 10       | 1  | 0               | 0                   | -1                              |
| 11       | -1 | 0               | 0                   | 1                               |
| 12       | 1  | 0               | 0                   | 1                               |
| 13       | 0  | -1              | -1                  | 0                               |
| 14       | 0  | 1               | -1                  | 0                               |
| 15       | 0  | -1              | 1                   | 0                               |
| 16       | 0  | 1               | 1                   | 0                               |
| 17       | -1 | 0               | -1                  | 0                               |
| 18       | 1  | 0               | -1                  | 0                               |
| 19       | -1 | 0               | 1                   | 0                               |
| 20       | 1  | 0               | 1                   | 0                               |
| 21       | 0  | -1              | 0                   | -1                              |
| 22       | 0  | 1               | 0                   | -1                              |
| 23       | 0  | -1              | 0                   | 1                               |
| 24       | 0  | 1               | 0                   | 1                               |
| 25       | 0  | 0               | 0                   | 0                               |
| 26       | 0  | 0               | 0                   | 0                               |
Results and discussion

FT-IR spectroscopy
In order to determine the composition of the surface, the FT-IR method was used. Figure 2 represents the FT-IR spectra of pristine Mn$_2$P$_2$O$_7$ and synthesized α-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ composite, which prepared using FHRC method. In the FT-IR spectrum of synthesized Mn$_2$P$_2$O$_7$, there was a strong absorption for Mn$_2$P$_2$O$_7$ sample at 1094 cm$^{-1}$, which was ascribed to asymmetric stretching of PO$_2$ unit. The bands at 736 cm$^{-1}$ and 950 cm$^{-1}$, which appeared in the pristine Mn$_2$P$_2$O$_7$ material spectrum was due to the stretching vibration of P-O bond and symmetric or asymmetric stretching mode of P-O-P tertiary group, respectively [15]. The bands at 1600 cm$^{-1}$ and 3500 cm$^{-1}$ in the spectrum of the synthesized composite were related to bending and stretching vibrating modes of O-H bond, respectively. The peaks at around 482 cm$^{-1}$ and 886 cm$^{-1}$ were ascribed to vibration mode of Fe-O bond [16]. Other changes in the spectral range from 400 to 500 cm$^{-1}$ represents the formation of new bonds in the synthesized composite.

![FT-IR spectra of synthesized compounds](image)

Figure 2. FT-IR spectra of synthesized compounds

Powder X-ray diffraction
XRD pattern of the synthesized α-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ composite was displayed in Figure 3. This pattern exhibited (111), (-201), (130), (131) and (-311) Bragg reflections at 2θ = 28.96, 30.36, 34.41, 41.61 and 43.71, which were in good agreement with powder diffraction data and attributed to the monoclinic structure of Mn$_2$P$_2$O$_7$. Furthermore, some additional peaks were observed for the synthesized α-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ composite at 2θ = 24.11, 33.06, 35.66, 49.26 and 54.0 which were assigned to planes of (012), (104), (110), (024) and (116) in the rhombohedral (hexagonal) structure of α-Fe$_2$O$_3$ (space group: R-3c) [17].
Synthesis and characterization of nano $\alpha$-$\text{Fe}_2\text{O}_3$/M$_2\text{P}_2\text{O}_7$ for photocatalytic...

![Figure 3. XRD pattern of synthesized $\alpha$-$\text{Fe}_2\text{O}_3$/M$_2\text{P}_2\text{O}_7$](image)

**Scanning electron microscopy**

The morphology of synthesized composite was investigated using SEM technique (Figure 4). The SEM image of the prepared $\alpha$-$\text{Fe}_2\text{O}_3$/M$_2\text{P}_2\text{O}_7$ nanocomposite displayed that the surface of M$_2$P$_2$O$_7$, which acts as the support for the photocatalyst, was obviously decorated by numerous metal oxide particles with a typical diameter of less than 90 nm. The catalytic $\alpha$-$\text{Fe}_2\text{O}_3$ nanoparticles, which were synthesized using the FHRC method, were dense and close to each other on the surface.

![Figure 4. SEM images of (a) synthesized M$_2$P$_2$O$_7$ and (b) synthesized $\alpha$-$\text{Fe}_2\text{O}_3$/M$_2\text{P}_2\text{O}_7$ composite](image)

**Energy dispersive X-ray analysis**

EDX method was used to detect the presence of the elements and also to determine the amount of them in the synthesized composite. Figure 5 shows the EDX spectrum of the synthesized composite. The obtained spectrum proves the presence of oxygen, phosphorus, iron and manganese elements in the synthesized composite. These obtained data and values confirmed that $\alpha$-$\text{Fe}_2\text{O}_3$/M$_2\text{P}_2\text{O}_7$ composite was formed.
Surface area measurement using the BET method
The specific surface areas of the α-Fe₂O₃/Mn₂P₂O₇ composite and Mn₂P₂O₇ have been measured. The obtained isotherms are shown in Figure 6. The adsorption-desorption isotherms of these materials showed a hysteresis loop classified as type IV by IUPAC. The specific surface area of the solid support was 125 m²/g. when the composite was formed, the surface area increased to 160 m²/g. This increase in surface area is due to the presence of the α-Fe₂O₃ nanoparticles on the surface of Mn₂P₂O₇.

In accordance with the results presented in the literature [18], a schematic of the proposed photocatalytic mechanism is shown in Figure 7 and the main stages are numbered. In the first stage, the photons from the UV light are absorbed by the α-Fe₂O₃ photocatalyst, which causes the electrons in the valence band to be transferred to the conduction band and thus form electron-hole pairs. In the second step, some electrons and holes are recombined again and the energy is lost in the form of heat. The third stage is the beginning of the process of oxidation by the cavities in the valence band that produce hydroxyl radicals. In the fourth stage, the
reduction process is performed by excited electrons, which are placed in the conduction band. Finally, photocatalytic reactions are conducted to decompose contaminants and produce mineral products. In this way, hydroxyl radicals attack to the contaminating molecules and degrade them chemically. The process details are summarized in the following chemical equations:

\[ \alpha-Fe_2O_3 + hv \rightarrow \alpha-Fe_2O_3 (e^-_{CB} + h^+_{vb}) \]
\[ h^+_{vb} + H_2O \text{ (ads)} \rightarrow H^+ + OH^-\text{(ads)} \]
\[ e^-_{CB} + O_2 \text{ (ads)} \rightarrow O_2^-\text{(ads)} \]
\[ H_2O \rightarrow H^+ + OH^- \]
\[ 2O_2^-\text{(ads)} + H^+ \rightarrow HO_2^- \]
\[ H_2O_2 + \alpha-Fe_2O_3 (e^-_{CB}) \rightarrow OH + OH^- + \alpha-Fe_2O_3 \]
\[ \alphaOH\text{(ads)} + p-Xylene \rightarrow \text{Degradation of p-Xylene} \]
\[ h^+_{vb} + p-Xylene \rightarrow \text{Oxidation of p-Xylene} \]

Figure 7. A proposed mechanism of the photocatalytic process

**Design of experiments and statistical analysis**

Analysis of variance (ANOVA) is a collection of a number of statistical methods used in the analysis of the difference between the mean of groups and the related methods. ANOVA is used to test the meaningfulness of the mean of three or more variables. Also, this method is used for graphical data analysis to obtain the interaction between process variables and response. The quality of the polynomial model is expressed through the coefficient of determination of \( R^2 \) and the significance of the coefficients is determined using F-test (Fisher test). The components of the model are evaluated through P-Value. Table 3 presents the estimated effects and coefficients of each model component for the response variable (X%). In this table, the standard error of estimation (S), coefficient of determination (\( R^2 \)), adjusted coefficient of determination (\( R^2 \text{ adjusted} \)) and prediction coefficient (\( R^2 \text{ Pred} \)) have also been reported. The square of the correlation coefficient is calculated as the coefficient of determination (\( R^2 \)) for the response variable. The accuracy and diversity of the model are evaluated through \( R^2 \). The value of \( R^2 \) is always between 0 and 1. When \( R^2 \) is close to 1, indicate higher power of the model in the determination of the X% variable and its better prediction. In this research, the obtained value of \( R^2 \) was 99.55%.
According to Table 3 and the significant effect of variables on the process, the magnitude of the effects of pH, concentration of H$_2$O$_2$, concentration of catalyst and Initial concentration of p-Xylene variables were obtained -2.908, 1.287, 4.145, and -14.89, respectively. Therefore, the reaction parameters (from highest to lowest effect) were p-Xylene concentration, catalyst concentration, pH and H$_2$O$_2$ concentration, respectively. It should be noted that despite the two variables of H$_2$O$_2$ concentration and catalyst in the model, the effect of pH (-2.908) and concentration of p-Xylene (-14.89) was negative in the model. It means that increasing the initial concentration of p-Xylene or pH will result in reduced efficiency. In this way, the interactive effects of variables are reported in Table 3.

| Term                        | Coef | SE Coef | T (Coef/SE Coef) | P value | Result |
|-----------------------------|------|---------|-------------------|---------|--------|
| Constant                    | 78.41| 0.628   | 124.9             | 0.000   | Significant |
| pH                          | -2.908| 0.314  | -9.27             | 0.000   | Significant |
| H$_2$O$_2$ con.             | 1.287| 0.314   | 4.1               | 0.001   | Significant |
| Catalyst con.               | 4.145| 0.314   | 13.2              | 0.000   | Significant |
| Initial con. of P-Xylene    | -14.89| 0.314  | -47.43            | 0.000   | Significant |
| pH X pH                     | -0.556| 0.471  | -1.18             | 0.260   |         |
| H$_2$O$_2$ con. X H$_2$O$_2$ con. | 0.799| 0.471  | 1.7               | 0.116   |         |
| Catalyst con. X Catalyst con. | -0.089| 0.471  | -0.19             | 0.854   |         |
| Initial con. of P-Xylene X Initial con. of P-Xylene | -4.556| 0.471 | -9.68             | 0.000   | Significant |
| pH X H$_2$O$_2$ con.        | -0.893| 0.544   | -1.64             | 0.127   |         |
| pH X Catalyst con.          | -0.227| 0.544   | -0.42             | 0.683   |         |
| pH X Initial con. of P-Xylene | 0.544| 1.55   | 0.146             | 1.000   |         |
| H$_2$O$_2$ con. X Catalyst con. | -1.442| 0.544  | -2.65             | 0.021   | Significant |
| H$_2$O$_2$ con. X Initial con. of P-Xylene | 0.095| 0.544  | 0.17              | 0.864   |         |
| Catalyst con. X Initial con. of P-Xylene | 1.83 | 0.544 | 3.37              | 0.006   | Significant |

As can be seen, the only dual interaction between the catalyst and the concentration of p-Xylene has a positive effect on the response. The second-order effects of P-Xylene X P-Xylene and the interaction of H$_2$O$_2$ X Catalyst in the model are negative and significant. It should be noted that the obtained P-values for each of the model components in Table 3 are measured according to the considered error level (α = 0.05). Table 4 shows the results of the ANOVA. The effect of each parameter on the response variable increases with increasing F-value and decreasing the P-value. For the main effects (with 4 degrees of freedom), including the initial concentration of P-Xylene, pH, H$_2$O$_2$ concentration and catalyst concentration, F and P values were determined to be 631.77 and P <0.0001, respectively. In addition, F and P values for second-order effects were 31.27 and P <0.0001 respectively and for interactive interactions, values of 3.95 and 0.021 were obtained.
Synthesis and characterization of nano $\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ for photocatalytic ...
Table 5 contains additional results, which were used for the residual plot. As can be seen, the actual and predicted values are very close together. Another method, which is very useful for checking the distribution of residues is plotting the normal probability plot (P-plot). If the distribution of residues is normal, the plot is similar to a straight line.

Figure 8 (a) shows the normal probability plot. In this plot, it is clear that the distribution of residues is normal due to the fact that all the points are close to the straight line. If the model is correct and if the assumptions have been met, the residues should not have a particular trend. In particular, they should not correlate with any other variables including the fitted variables. The evaluation of this issue carried out using the plot of the residual values against fitted values.

Figure 8 (b) shows the plot of residuals against fitted values. As can be seen, the residual plot versus the fitted values has non-uniformity and does not show any particular trend. According to Figure 8 (C), the abundance diagram of residual values indicates the relatively normal distribution of the residuals. In order to better understand the residual values, the residual plot is shown against the observed values in Figure 8 (d). As seen, 15 points (residues) are located below the line (negative) and 12 points above the line. According to this point and comparing the distance from the zero line, it can be stated that the distribution of the residues is normal.

The mathematical model that shows the efficiency of p-Xylene removal in this research is given in the following Equation:

\[
\text{Degradation\%} = 82.5 + 0.10(pH) + 30.1(H_2O_2) + 0.051(Cat) + 0.230(p - xylene) - 0.139(pH)^2 + 20.0(H_2O_2)^2 - 0.000099(Cat)^2 - 0.005062(p - xylene)^2 - 2.32(pH \times H_2O_2) - 0.00379 (pH \times Catalyst ) + 0.01408(pH \times p - xylene) - 0.2404(Cat \times H_2O_2) + 0.0158(H_2O_2 \times p - xylene) + 0.002033(Cat \times p - xylene)
\]

![Figure 8](image.png)

**Figure 8.** (a) Normal probability plot, (b) plot of residuals versus fitted values, (c) Histogram of residuals, (d) plot of residuals versus observation order
Figure 9 shows the main effects graphs. Based on these graphs, from the four main parameters, the effect of two pH and p-Xylene parameters on the response variable (p-Xylene removal efficiency) is negative. The effect of two catalysts and H₂O₂ parameters is positive. The slope of the line in the main graph is an indicator of the magnitude of independent variable effects on the process. Therefore, the effective variables are p-Xylene, catalyst, pH and H₂O₂, respectively.

Figure 9. Main effect plot for actual degradation (%)

In Figure 10, the interactive effects of variables on the efficiency of xylene removal have been investigated. As can be seen, there is a significant interactive effect between catalyst concentration and H₂O₂ concentration. In addition, there is a higher interactive effect between the catalyst and the concentration of p-Xylene.

Figure 10. Interaction plot for actual degradation (%)

Page 71
It is easy to detect the optimum condition of the experiment through plotting response surface and contour graphs. Figure 11 shows the response level graph for the experiment variables. Figure 11 (a) shows the three-dimensional response graph of the resulting regression model, assuming a constant pH and H$_2$O$_2$ concentration in values of 7 and 0.3 ppm, respectively. As seen in this figure, the highest removal efficiency occurs at a concentration of 120 ppm of catalyst and a concentration of 70 ppm P-Xylene. In addition, by reducing the concentration of catalyst and increasing the concentration of p-Xylene, the efficiency of the removal of p-Xylene decreases. Figure 11 (b) shows the three-dimensional graph, assuming a constant pH and catalyst in values of 7 and 90 ppm, respectively. The optimum removal point for P-xylene concentration is 70 ppm and for H$_2$O$_2$ concentration is 0.5 ppm. The results also indicate that the removal efficiency is more dependent on P-Xylene than on H$_2$O$_2$ concentration. Figure 11 (c) shows the three-dimensional response surface graph with the assumption of constant pH and p-Xylene in the values of 7 and 100 ppm, respectively. The most effective removal of p-Xylene, in this case, occurred in the catalyst concentration of 120 ppm and H$_2$O$_2$ of 0.5 ppm. Figure 11 (d) shows the three-dimensional response graph, with the assumption that H$_2$O$_2$ and catalyst are kept constant in the values of 0.3 ppm and 90 ppm, respectively. In the pH of 5 and p-Xylene concentration of 70 ppm, the most effective removal of p-Xylene occurs. Moreover, Figure 11 (e) illustrates the three-dimensional graph with the assumption that H$_2$O$_2$ and p-Xylene are kept constant at values of 0.3 ppm and 100 ppm, respectively. The results showed that the highest efficiency for xylene removal in a pH of 5 and catalyst concentration of 120 ppm was obtained. Figure 11 (f) shows the three-dimensional response graph of the resulting regression model, assuming a constant catalyst and P-Xylene concentration in values of 90 ppm and 100 ppm, respectively. The most effective removal of xylene is achieved in pH values of 5 and H$_2$O$_2$ concentration of 0.5 ppm.
The results of the contour graphs are shown in Figure 12. The Figure 12 (a) shows the changes in the efficiency of p-Xylene removal by maintaining the pH and H$_2$O$_2$ at levels of 7 and 0.3. As can be seen, with the increase in the amount of p-Xylene, the efficiency of removal is reduced and by increasing the amount of catalyst, the efficiency is increased. Figure 12 (b) shows the changes in the efficiency of the p-Xylene removal by keeping the pH and catalyst values constant at levels of 7 and 90 ppm. According to the results, with a decrease in the amount of P-Xylene, removal efficiency is increased. In addition, the efficiency of the removal of p-Xylene, in the range of 0.1 to 0.4 ppm of H$_2$O$_2$ concentration, remains constant. While the utilized amount of H$_2$O$_2$ was 0.5 ppm, removal efficiency increased. Figure 12 (c) shows the changes in the efficiency of the p-Xylene removal by keeping the pH and P-Xylene concentration fixed at levels of 7 and 100. The results indicate that by increasing the catalyst and H$_2$O$_2$ concentrations, the efficiency of the p-Xylene removal increases. Figure 12 (d) shows the changes in the efficiency of the p-Xylene removal by keeping the two variables of H$_2$O$_2$ and catalyst fixed at the levels of 0.3 ppm and 90 ppm. The results indicate that by decreasing the pH and p-Xylene values,
The efficiency of the removal process increased. Figure 12 (e) shows the changes in the efficiency of p-Xylene removal by keeping the two variables of H$_2$O$_2$ and P-Xylene fixed at levels of 0.3 ppm and 100 ppm. The results indicate that by decreasing the pH and increasing the catalyst concentration, process efficiency increases. Figure 12 (f) shows the changes in the efficiency by keeping the two variables of catalyst and p-Xylene fixed at 90 ppm and 100 ppm. As can be seen, the efficiency of p-Xylene removal increases with decreasing pH and increasing the amount of H$_2$O$_2$.

Figure 12. Contour plot for actual degradation (%)
In order to fully evaluate and investigate the effect of support on the photocatalytic activity, pure $\alpha$-Fe$_2$O$_3$ was also used. For this purpose, all of 27 experiments that were designed for the $\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ composite were also studied for the pure $\alpha$-Fe$_2$O$_3$ species. The obtained results, which are summarized in Table 6 shows that $\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ composite has better performance than $\alpha$-Fe$_2$O$_3$ species in the degradation process of p-Xylene. This indicates that the presence of the Mn$_2$P$_2$O$_7$ support prevents the particles aggregation. Therefore, the presence of support will increase the surface area of the photocatalytic nanoparticles.

| Exp. No. | Pure $\alpha$-Fe$_2$O$_3$ | $\alpha$-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ |
|----------|--------------------------|----------------------------------|
| 1        | 69.89                    | 79.22                            |
| 2        | 65.13                    | 76.45                            |
| 3        | 72.61                    | 83.45                            |
| 4        | 67.14                    | 77.11                            |
| 5        | 74.15                    | 85.78                            |
| 6        | 83.82                    | 91.17                            |
| 7        | 40.41                    | 53.51                            |
| 8        | 55.83                    | 66.22                            |
| 9        | 85.23                    | 93.38                            |
| 10       | 72.77                    | 84.11                            |
| 11       | 53.54                    | 61.27                            |
| 12       | 45.43                    | 55.38                            |
| 13       | 62.32                    | 72.61                            |
| 14       | 67.41                    | 78.69                            |
| 15       | 71.54                    | 82.91                            |
| 16       | 72.31                    | 83.22                            |
| 17       | 61.22                    | 75.35                            |
| 18       | 60.98                    | 70.49                            |
| 19       | 73.17                    | 84.21                            |
| 20       | 67.97                    | 78.44                            |
| 21       | 79.55                    | 88.22                            |
| 22       | 81.42                    | 90.11                            |
| 23       | 47.21                    | 57.72                            |
| 24       | 51.78                    | 59.99                            |
| 25       | 67.23                    | 78.45                            |
| 26       | 67.45                    | 78.16                            |
| 27       | 67.92                    | 78.62                            |

*Optimization of conditions*

The exact values of the optimal variables are shown in Table 7. In order to assess the accuracy of the prediction, that was performed using the Minitab 18 software, p-Xylene removal process was performed in the predicted optimal conditions (i.e.; $\text{pH}=5$, $\text{C}_{\text{H}_2\text{O}_2}=0.5$ ppm, $\text{C}_{\text{Catalyst}}=120$ ppm, and $\text{C}_{\text{p-Xylene}}=70$ ppm). The experimental result obtained in optimal conditions was 96.68% for p-Xylene removal, which was close to the predicted value of 95.84%. The proximity between the experimental and the predicted values represents the validity of the existing model. This shows that RSM is a powerful tool for determining the exact values of the optimal conditions [19].
Table 7. The optimum value of the process parameters

| pH | Cr(VI) (ppm) | Catalyst (ppm) | C p-Xylene (ppm) | Efficiency (%) |
|----|-------------|----------------|------------------|---------------|
| 5  | 0.5         | 120            | 70               | 96.68         |

**Conclusion**

In summary, α-Fe₂O₃/Mn₂P₂O₇ composite as an efficient photocatalyst was prepared using forced hydrolysis and reflux condensation method (FHRC). Based on the results of XRD, EDAX, FT-IR, BET, and SEM, it was found that α-Fe₂O₃ nanoparticles were decorated on the Mn₂P₂O₇ surface. AOPs (α-Fe₂O₃/Mn₂P₂O₇, UV/H₂O₂) as a solution-based method was used to investigate the photodegradation process of p-Xylene. Results of the photocatalysis experiment showed that the photodegradation efficiency appeared to reach 96.68% in 90 min. According to the literature, it can be suggested that ‘OH species are the most effective agents, which control the reaction mechanism. In comparison with non-supported α-Fe₂O₃ nanoparticles, the heterogeneous system had better performance due to the distribution of particles on the surface of the manganese pyrophosphate that prevents the accumulation of nanoparticles. The heterogeneity and recyclability of the photocatalyst system, along with the proper efficiency of the catalyst, are the most important features of the synthesized catalyst.

**Acknowledgments**

The authors thank the Arak Azad University for laboratory facilities.

**References**

[1] D. Wu, X. Quan, Y. Zhao, S. Chen, J. Hazard. Mater., 2006, 136, 288-295.
[2] (a) H. Hong-Sheng, S. Hao, Z. Ya-Jin, Commun. Theor. Phys., 2013, 59, 443-446; (b) M. Almasi, Chem. Methodol., 2018, 2, 308-314; (c) A. Khazaei, M.A. Zolfigol, M. Mokhlesi, F.D. Panah, S. Sajjadifar, Helvetica Chimica Acta., 2012, 95, 106-114.
[3] H. Elmrini, N. Bredin, Z. Shareefdeen, M. Heitz, Chem. Eng. J., 2004, 100, 149-158.
[4] B. Bühler, B. Witholt, B. Hauer, A. Schmid, Appl. Environ. Microbiol., 2002, 68, 560-568.
[5] (a) H. Salavati, A. Teimouri, S. Kazemi, Chem. Methodol., 2017, 2, 158-169; (b) H. Salavati, A. Teimouri, S. Kazemi, Chem. Methodol., 2017, 1, 12-27; (c) C. Ye, K. Hu, Z. Niu, Y. Lu, L. Zhang, K. Yan, J. Water. Process. Eng., 2019, 27, 205-210.
[6] M. Mishra, D.-M. Chun, Appl. Catal. A. Gen., 2015, 498, 126-141.
[7] (a) W.E. John, A.A. Ayi, C. Anyama, P.B. Ashishie, B.E. Inah, Adv. J. Chem. A., 2019, 2, 175-183; (b) S. Deljoo, N. Rabiee, M. Rabiee, Asian J. Nanosci. Mater., 2019, 2, 66-91; (c) P. Gharbani, A. Mchalizadeh, Asian J. Nanosci. Mater., 2019, 2, 27-36.
[8] (a) F. Moeinpour, A. Khojastehnezhad, Chin. Chem. Lett., 2015, 26, 575-579; (b) P. Torabian, F. Ghandehari, M. Fatemi, Asian J. Green Chem., 2018, 2, 181-188; (c) E. Teymoori, A. Davoodnia, A. Khojastehnezhad, N. Hosseininasab, Iran. Chem. Commun., 2019, 7, 271-282; (d) B. Maleki, N. Nasiri, R. Tayebee, A. Khojastehnezhad, H.A. Akhlaghi, RSC Adv., 2016, 6, 79128-79134; (e) B. Maleki, M. Baghayeri, S.A.J. Abadi, R. Tayebee, A. Khojastehnezhad, RSC Adv., 2016, 6, 96644-96661.
Synthesis and characterization of nano α-Fe$_2$O$_3$/Mn$_2$P$_2$O$_7$ for photocatalytic decomposition of p-xylene using Box-Behnken design. 

Saijead Mafi, Kazem Mahanpoor. Eurasian Chemical Communications, 2020, 2(1), 59-77.