Estimation of aerodynamic noise of diaphragms through IEC 60534-8-3 and CFD

Luca Fenini, Luca Nicola Quaroni and Stefano Malavasi

Abstract
The aerodynamic noise emitted by a subsonic flow of dry air through an orifice plate is estimated in terms of internal sound power level and external sound pressure level (SPL) by application of the methodology described in the international standard IEC 60534-8-3. A shortcoming of the standard in defining the efficiency of the transformation of the mechanical energy of the flow into acoustic energy is discussed. Experimental evidence of the matter is also described. An alternative model employing the resolution of Reynolds Averaged Navier-Stokes equations (RANS) by means of Computational Fluid Dynamics (CFD) techniques for the calculation of the acoustic power generated by the turbulent flow through the orifice plate is applied so as to overcome the issue.

Keywords
Aerodynamic noise, orifice plate, acoustic power, CFD

Date received: 24 September 2020; accepted: 21 December 2020

Introduction
Aerodynamic noise in flow-regulating devices (e.g. valves, flow-measuring diaphragms) is generated by the turbulent flow of a gas through the inner body of the element and it’s a well-known problem in such fields as Oil & Gas (O&G) or Heating, Ventilation and Air Conditioning (HVAC). In fact, the noise emissions so caused may reach hazardous levels for the health of the work personnel in the neighborhood of the device. Furthermore, the aerodynamically generated sound pressure field downstream of the regulator may cause structural damages to the piping system if its frequency content is close enough to the natural one of the latter.1 High enough levels of the overall sound pressure fluctuations independent of the frequency distribution are also known to be the source of structural problems.2

Even though the practical importance of the topic is paramount, the coexistence of many different physical phenomena (turbulence, self noise, sound transmission along and through the pipe’s walls and propagation of the acoustic pressure through the surrounding medium) make the task of predicting noise emissions by flow-control devices a highly complex one.

Interest in the discipline steadily arose since the end of the 1960s, when the advancement in the field of aeroacoustics applied to jet engines pioneered by the works of Lighthill3,4 shed a new light on the phenomenon. Due to the intrinsic difficulty of the subject, most of the early research in control flow devices has been experimental in nature. Among the earliest works one may cite the experimental campaign by Jenvey5 on the aerodynamic noise generated by flow through simple orifice plates placed in circular ducts. In his work, Jenvey derived a relationship between the applied pressure drop across the valve and the acoustic power emitted by the orifice. He did so by a rewriting of the formulation obtained through dimensional reasoning and experimental campaigns by Lighthill for free turbulent jets, therefore assuming a quadrupole-like source for the aerodynamic noise of control devices. The theoretical results closely followed those obtained by an experimental campaign. However, Blake6 later contested that the orifice plates employed in Jenvey’s work had too small of a hole-to-pipe diameter ratio, therefore favoring the quadrupole source linked to turbulence proper over the dipole source due to the interaction with the solid surfaces. This last observation may be of particular importance for the case of subsonic flows, as demonstrated by Nelson and Morfey.7 In
their work, the noise issuing from spoilers in rectangular ducts, commonly found in the HVAC sector, was studied in detail. In particular, the authors argued that the main contribution to noise generation is the dipole distribution caused by the exchange of a fluctuating drag force between the fluid and the orifice surface. By making the hypothesis that the fluctuating component of such force is directly proportional to the steady-state one through a generalized spectrum, they were able to compute the sound pressure level (SPL) generated by a series of rectangular spoilers of various widths. An experimental campaign validated their results. Other authors followed the lead of Nelson and Morfey’s work, demonstrating the validity of the dipole-type source for low Mach number flows.8–11

The previous review of the literature highlights the fact that the precise mechanism of sound generation by control devices is still to some degree unaccounted for. It is in this context that the International Electrotechnical Commission (IEC)12 issued a standard, the IEC 60534-8-3, currently in its third revised form, which provides a method to estimate the sound production of control devices through the knowledge of their sizing coefficients and working conditions.13 The standard draws from the body of knowledge on the subject by combining the results from the theory of Lighthill standard draws from the body of knowledge on the subject by combining the results from the theory of Lighthill...

IEC 60534-8-3 summary

The scope of the standard is the estimation of the external noise emitted by flow-control devices installed along a pipeline where a single-phase gas is flowing. In particular, the noise emissions are expressed in terms of the SPL at a point located 1 m far from the pipe’s external walls and 1 m downstream of the valve’s outlet. Its definition is:

$$SPL = 20 \log_{10} \left( \frac{p_{rms}}{p_{ref}} \right)$$

where $p_{rms}$ is the root mean square of the pressure fluctuations and $p_{ref}$ is a reference value of pressure corresponding to $2 \times 10^{-3}$ Pa. The SPL is measured in A-weighted decibels or dB(A), thus taking into account the human ear’s preferred sensitivity to a particular frequency range.13 For its application, the standard requires the description of a control device in terms of certain fluid dynamic and acoustic parameters as well as the hydraulics of the system (applied pressure differential $\Delta p$, upstream absolute pressure $p_1$, temperature $T$), the flowing fluid’s properties (inlet density $\rho_1$ and specific heat ratio $\gamma$) and the pipe’s structural properties (diameter $D$, thickness $s$, and density $\rho_p$). All hydraulic quantities are measured 2D upstream of the device and 6D downstream of it.

With regards to the fluid-dynamic characterization of the device, the standard makes use of the flow coefficient $C_f$, liquid pressure recovery factor $F_L$ and the valve style modifier $F_d$. In particular, the $C_f$ coefficient indicates the resistance opposed by the device to the flow and it is expressed in the non-I.S. units of $[gpm/psi^{0.5}]$. The non-dimensional $F_L$ factor is an indicator of a valve’s capability of converting kinetic energy back into pressure energy at its exit. Its values are limited to the range $[0,1]$ and the closer to unity the less efficient the valve is at recovering kinetic energy, which is thus dissipated into turbulent kinetic energy. Finally, the non-dimensional $F_d$ coefficient takes into account the deviation of the mean flow downstream of the valve from the benchmark case of a round jet; its value being equal to 1 for simple orifice plates and less than one for all other geometries of the flow passage area. The
evaluation of these parameters is performed according to another part of the standard IEC 60534 and can be dealt with either through experimental or numerical procedures.

The acoustic characterization of the device is described in the standard in terms of the already mentioned nondimensional valve correction factor for acoustical efficiency $A_h$ and the Strouhal number for peak frequency $St_p$. The former is involved in the expression of the efficiency of the transformation of part of the mechanical energy into acoustic energy, that is, the acoustical efficiency $\eta$. The latter is involved in computing the peak frequency of the acoustic pressure fluctuations downstream of the pipe. The standard states that these values could depend both on the geometry of the device and on the flow conditions, that is, the applied pressure differential $\Delta p$, the temperature $T$, the absolute upstream pressure $p_1$. Unlike for the fluid-dynamic coefficients however, no test procedures are proposed for their evaluation, but instead constant values are listed for the most common flow-control devices available on the market.

Figure 1 summarizes the main steps of the procedure and the role played by the four mentioned parameters in the noise computation.

The $F_l$ and the $C_V$ are employed in the evaluation of the mechanical power $W_m$ of the flow together with the hydraulic input data. A small portion of $W_m$ is converted into acoustic power $W_a$ because of turbulence: the ratio of the acoustic to mechanical power is defined as the aforementioned acoustic efficiency $\eta = W_a/W_m$. Based on the differential pressure ratio $x = \Delta p/p_1$, five different regimes of noise generation are defined by the standard. The present paper is limited to regime I, whereby subsonic conditions are present both in the upstream and the downstream branches of the pipe. For such regime, the expression for the acoustic efficiency is:

$$\eta = 10^{A_h F_l^2 M_{vc}^2}$$

where $M_{vc}$ is the Mach number in the vena contracta, itself a function of $F_l$, and of the specific heats of the flowing gas $\gamma$ through the formula:

$$M_{vc} = \sqrt{\left(\frac{2}{\gamma-1}\right) \left[\left(1 - \frac{x}{F_l^2}\right)^{\gamma - 1} - 1\right]}$$

The fundamental role played by the $A_h$ coefficient is clear, as it appears as the exponent in (2) and is therefore the most important parameter in defining the amount of mechanical energy which is radiated as sound downstream of the pipe. The transmission of sound through the pipe’s walls is dealt with by the standard through a decomposition of the noise in frequency bands, for which the filtering effect of the pipe is applied; the $St_p$ is involved in such decomposition. Finally, the SPL at 1 m downstream of the valve and at 1 m far from the pipe is computed by assuming a cylindrical propagation of sound in the outside environment.

**Parameters for acoustical characterization**

As flow-control devices regulate the flow by forcing the passage of a fluid through one or multiple constrictions, the flow at the outlet can be usually described as the interaction of one or multiple closed jets. Indeed, jets are one of the most studied configurations in aeroacoustics, either freely expanded or enclosed. As such, the chosen benchmark configuration for the work presented in the paper is that of a perforated plate whose axis is aligned with the pipe’s one, reported in Figure 2. The sensitivity of the predicted noise levels on the two acoustic parameters $A_h$ and $St_p$ is first performed.

The design of the tested orifice is the one described in the ISA international standard (Figure 2). This was done in order to remove any uncertainty relative to the
values of the fluid-dynamic parameters $C_V$, $F_L$, and $F_d$. The values of such parameters and the ones suggested by the IEC for the acoustical ones are reported in the following Table 1:

In particular, the values suggested by the IEC for $A_h$ and $St_p$ are those of a generic perforated plate configuration, with no regards to its design (sharp- or round-edged, number of perforations, thickness of the plate). The sensitivity analysis presented in the next section is thus finalized to the evaluation of the effect of these parameters’ uncertainty on the external noise and to the identification of the parameter which most affects the SPL prediction.

### Table 1. Characterizing parameters for the ISA orifice plate, from ISA and IEC 60534-8-3.

| Parameter | Value | Units |
|-----------|-------|-------|
| $C_V$ | 52 | [gpm/psi$^{0.5}$] |
| $F_L$ | 0.86 | - |
| $F_d$ | 1 | - |
| $A_h$ | -4.8 | - |
| $St_p$ | 0.2 | - |

### Noise sensitivity on the acoustic parameters

The influence of $A_h$ and $St_p$ on the SPL is investigated at varying differential pressure ratios employing for the two parameters values in the ranges found in the IEC standard and the equations (2) and (3). The calculations are conducted with constant upstream absolute pressure $p_1 = 5.2$ barA and with a pressure drop $\Delta p$ going from 0.1 bar to 1.3 bar, the latter corresponding to a jet Mach number close to 0.8. The IEC ranges for the two parameters are $A_h\in [-4.8,-3]$ and $St_p\in [0.19,0.3]$. In Figure 3 the SPL obtained at different pressure ratios $x$ and the variability of the results with the values of $A_h$ and $St_p$ are shown. In particular, the base curve (in black) is that obtained employing $A_h = -4$ and $St_p = 0.2$.

The sensitivity of the SPL on the value of $A_h$ is much greater than the one on $St_p$. In fact, differences of up to 18 dB(A) are measured due to the different values of $A_h$ employed, while the variation due to $St_p$ is limited to no more than 3.6 dB(A). It can be shown that a variation on $A_h$ of 0.1 induces a change in the predicted external noise of 1 dB. Because of the major influence of the valve correction factor for acoustical efficiency on the noise, the following sections are devoted to the analysis of an acoustic model for the derivation of $A_h$ which considers its variation with the flow conditions.

### Experimental evidence of $A_h$ dependency on flow conditions

The assumption of a constant value of the valve correction factor for acoustical efficiency $A_h$ was shown to underestimate the actual values of SPL. In particular, Mazzaro measured the SPL of a perforated plate (of a different geometry than the one subject of this paper) inside an anechoic chamber according to the prescriptions outlined in the IEC standard. The results are reported in Figure 4, which shows the measured SPL for varying $x$ together with the estimated one using $A_h = -4.8$ (orifice plates) and $A_h = -4$ (dipole sources). The experimental data shows that the IEC underestimates the emitted noise and in particular the prediction with $A_h = -4.8$ is always more than 10 dB lower than the recorded SPL. As expected from the previous consideration about the influence of $A_h$ on the SPL, the two IEC series are just shifted of 8 dB because they are computed with two $A_h$ that differ of 0.8. It is thus possible to observe that a constant difference in the valve correction factor for acoustical efficiency returns a constant shift of the noise curves. Unlike the IEC data, the experimental results are not shifted by a constant quantity; instead, they get closer and closer to the results obtained for $A_h = -4$ as $x$ increases. This is indirect evidence of the fact that the $A_h$ factor is not constant with the flow, otherwise a constant shift with the IEC curves would have been observed.
Acoustic model for $A_{\eta}$ estimation

The $A_{\eta}$ factor can be obtained by inverting (2) once the acoustic efficiency $\eta$ is known. To be able to do this means having an expression for the acoustic power $W_a$ and the mechanical power $W_m$, being $\eta$ their ratio. The IEC formula for the mechanical power in noise generation Regime I is:

$$W_m = \frac{1}{2} Q_m (M_v c_w)^2$$  \hspace{1cm} (4)

where $Q_m$ is the mass flowrate and $c_w$ is the speed of sound in the vena contracta, for which the standard provides the formulas:

$$Q_m = 27.3 \left( 1 - \frac{x}{3x_T} \right) C_V \sqrt{\rho_1 \Delta p}$$

$$c_w = \sqrt{\frac{\gamma \rho_1}{\rho_1} \left( 1 - \frac{x}{x_T} \right) \frac{1}{C_0}}$$

with $x_T$ the choking pressure differential factor, computable either experimentally or numerically.

Since the IEC standard computes the acoustic power in terms of $\eta$ and $W_m$, and therefore in terms of $A_{\eta}$, a different model for such quantity is here used. In particular, the model of Proudman for the acoustic power density $P$ of a fluid subject to isotropically freely decaying turbulence in low Mach number flows is used.21 On the one hand the model presents the advantage of being able to describe the noise-generation mechanism in terms of the statistics of the turbulence, that is, the turbulent kinetic energy $K$ and the turbulent dissipation rate $\varepsilon$. These can be readily computed through numerical simulations solving the compressible RANS equations in the fluid domain. On the other hand however, the validity of the formulation in the case of the non-isotropic turbulence generated by control devices and the relatively high Mach numbers may be questionable. Furthermore, as the model was developed starting from Lighthill’s results for free turbulent jets, the possible dipole-nature of the noise generation mechanism is not considered. As for the assumption of freely decaying turbulence, Proudman himself questioned it stating that in such a case the turbulent energy dissipation may just be represented by the rate of introduction of energy in the flow in steady conditions. The expression for the acoustic power density is:

$$P = \alpha_P \varepsilon \left( \frac{\sqrt{2K/\varepsilon}}{v} \right)^5$$  \hspace{1cm} (5)

where $v$ is the speed of sound and $\alpha_P$ is a constant.

Different literature values for $\alpha_P$ have been suggested in the range $0.629\ldots13$; in this paper a re-scaled model that sets it equal to 3.804 is used.22 The total acoustic power can then be computed by integrating $P$ over an aptly defined source region:

$$W_a = \int_{S,R} P(x) dx^3$$ \hspace{1cm} (6)

The source region (S.R.) is defined in this paper according to Mesbah23 who considered it the flow region for which the turbulent kinetic energy $K$ is higher than 20% of the maximum value attained. The hat is here applied to distinguish the acoustic power estimated with Proudman’s formula from the value $W_a$ computed through the acoustical efficiency $\eta$. Inverting the estimation, the equation of the valve correction factor for acoustical efficiency is obtained:

$$A_{\eta} = \log_{10}\left( \frac{W_a}{P_2 M_v^2 W_m} \right)$$  \hspace{1cm} (7)

The described model for the acoustic power of the flow is applied for the computation of the $A_{\eta}$ factor for the ISA orifice plate described above for varying flow conditions. In particular, the RANS equations are used to retrieve the average characteristics of the turbulent flow field imposing the same differential pressure ratios as the ones imposed for the noise sensitivity analysis in Figure 3. The flow field is computed with compressible RANS simulations run on a three-dimensional domain without exploiting any geometrical symmetry.19 An hexahedral-type mesh was employed for improved convergence, while the ideal gas law was set as the constitutive equation for the fluid. The boundary conditions are specified in terms of total pressure at the inlet and static pressure at the outlet. Turbulence is modeled through the RNG $k-\varepsilon$ model, which returns the fundamental turbulent statistics required for the application of (4). The choice of such a turbulence model is based on previous studies indicating a better performance in case of sudden expansion of the flow.24

Results and discussion

The numerical acoustic power $\bar{W}_a$ so obtained is compared in Figure 5 to the one returned by application of the IEC procedure with $A_{\eta}$ equal to $-4$ and $-4.8$, that is, the values suggested for a generic dipole source and an orifice plate respectively. The acoustic power obtained through Proudman’s expression for $W_a$ is
between that computed using the two constant values. This suggests that the model in equation (5) may be reliable, since it returns a prediction which is consistent with the results suggested by the international standard IEC. Furthermore, all curves display the same qualitative behavior, that is, an exponential-like growth with $x$. Fenini also showed that for the two curves obtained using constant $A_n$ values, the acoustic power $W_a$ grows with the sixth-power of the mean flow velocity. From the theory of aeroacoustics, it is known that such a dependency on the flow velocity is characteristic of noise sources related to the exchange of forces with solid boundaries present in the flow. Lighthill’s theory however states that the acoustic power of the flow in a turbulent jet must be dependent on the eighth power of the mean flow velocity $U$. Since according to the IEC, for noise generation regime I:

$$W_a = \left(10^{A_n F_L F_d M_n^3} \right) \cdot W_m \rightarrow W_a \propto 10^{A_n} \cdot U^6 \tag{8}$$

the only way to make $W_a \propto U^6$ is to impose:

$$10^{A_n} \propto U^2 \rightarrow A_n \propto 2\log_{10} U \tag{9}$$

This theoretical analysis is confirmed by the graphical representation in Figure 6 of the $A_n$ curve obtained from $W_a$. In particular, $A_n$ shows a logarithmic relationship with the jet velocity $U$. For small pressure drops, $A_n$ is lower than $-4.8$ and it reaches that value only for a Mach number close to 0.4, corresponding to a flow with low compressibility effects. Further increasing the pressure drop and therefore the velocity, the $A_n$ factor increases logarithmically toward the value $-4$, suggesting that the acoustical efficiency $\eta$ of the orifice grows with the pressure drop.

The underestimation of $A_n$ for low Mach numbers is an acceptable error because in these flow conditions the compressibility effects are very weak and low noise generation is expected. This is confirmed by the analysis of the external noise computed in terms of SPL with $A_n$ (Figure 7). In fact, such value is lower than the one predicted by the standard for low pressure drops, and in particular for jet Mach numbers lower than 0.4. Even though this result means that Proudman’s model for the acoustic power is underestimating the noise emissions (nonconservative prediction), it must be highlighted that this error is committed for an external SPL that is lower than 40 dB(A) (corresponding to the noise intensity of a normal conversation), which is not the usual target in industrial applications. On the contrary, for significant noise levels, the prediction with $W_{ed}$ returns higher values than with $A_n = -4.8$, which is indicated as the characteristic value for perforated plates.

Conclusions

The procedure for the estimation of the acoustical emissions of a control-flow device according to an international standard (IEC 60534-8-3) was presented. In particular, emphasis was put on the five parameters characterizing the procedure. Three of them, that is, $C_V$, $F_L$, and $F_d$, can be computed with tests, either numerical or experimental in nature, proposed by the same standard. No guidelines are instead provided for the evaluation of the other two, that is, $A_n$ and $St_p$, for which only constant values are tabulated for the most common valve categories on the market. A sensitivity analysis of the external noise on the latter two showed that $A_n$, the valve correction factor for acoustical efficiency, is the one that most affects the SPL prediction.

An alternative procedure based on a literature model for the computation of the acoustic power from CFD simulations solving the compressible RANS equations was employed for estimating $A_n$ and predicting the emitted noise of a simple orifice subject to subsonic flow. The results showed that the obtained acoustic power lies between the values computed with the procedure suggested by the standard for a generic dipole source, $A_n = -4$, and for a generic perforated plate $A_n = -4.8$. The comparison of $W_a$ and $W_{ed}$ defines the curve of $A_n$, which shows a logarithmic proportionality to the flow velocity, resulting in an increase of the...
acoustical efficiency of the studied orifice with the applied pressure differential. The comparison of the external noise shows that the numerical prediction is lower than the IEC one only for SPL lower than 40 dB(A) (harmless noise) while it is in accordance with the IEC prediction for jet Mach numbers higher than 0.4. The results here presented are thus an advancement on the characterization of the $A_h$ parameter, because its variation with the pressure drop was described. The proposed approach based on CFD and on the Proudman model for $W_o$ may be extended to the prediction of $A_h$ for more complex devices.

Declaration of conflicting interests
The author(s) declared no potential conflicts of interest with respect to the research, authorship, and/or publication of this article.

Funding
The author(s) disclosed receipt of the following financial support for the research, authorship, and/or publication of this article: This project has been partly funded by Pibiviesse S.r.l, Nerviano (MI), Italy.

ORCID iD
Luca Nicola Quaroni ORCID iD 0000-0002-0673-8992

References
1. Sotoodeh K. Noise and acoustic fatigue analysis in valves. J Fail Anal Prev 2019; 19(3): 838–843.
2. Singleton EW. The impact of IEC 534-8-3 on control valve aerodynamic noise prediction. Meas Control 1999; 32(2): 37–44.
3. Lighthill J. On sound generated aerodynamically - I. General theory. Philos Trans R Soc London Ser A Math Phys Sci 1952; 211(1107): 564–587.
4. Lighthill J. On sound generated aerodynamically - II. Turbulence as a source of sound. Philos Trans R Soc London Ser A Math Phys Sci 1954; 222(1148): 1–32.
5. Jenvey I. Gas pressure reducing valve noise. J Sound Vib 1975; 41(4): 506–509.
6. Blake WK. Mechanics of flow-induced sound and vibration. Volume 2: complex flow-structure interactions. vol 2. 2nd ed. Academic Press, 2017.
7. Nelson P and Morfey C. Aerodynamic sound production. J Sound Vib 1981; 79(2): 263-289.
8. Oldham DJ and Ukropo AU. A pressure-based technique for predicting regenerated noise levels in ventilation systems. J Sound Vib 1990; 140(2): 259–272.
9. Tao F, Zhang X, Joseph P, et al. Experimental study of the mechanisms of sound generation due to an in-duct orifice plate. In: 21st AIAA/CEAS aeroacoustics conference, Dallas, TX, 22–26 June, 2015. American Institute of Aeronautics and Astronautics, Inc.
10. Laffay P, Moreau S, Jacob MC, et al. Experimental investigation of the noise radiated by a ducted air flow discharge though diaphragms and perforated plates. J Sound Vib 2020; 472: 115177.
11. Papaxanthos N, Perrey-Debain E, Ouedraogo B, et al. Prediction of air flow noise in ducts due to the presence of fixed obstacles. Euronoise 2015; (January): https://www.researchgate.net/publication/288975743_Prediction_of_air_flow_noise_in_ducts_due_to_the_presence_of_fixed_obstacles/citations
12. International Electrotechnical Commission (IEC). IEC 60534-3: industrial process control valves - noise considerations – control valve aerodynamic noise prediction method. IEC, 2010.
13. Baumann HD, Arant JB, Liptak BG, et al. Valves: noise calculation, prediction, and reduction. In: Instrument engineers handbook, fourth edition: process control and optimization, vol. 2, no. 1970. 2005, pp.1213–1233. CRC Press, a Taylor and Francis Group. https://www.routledge.com/Instrument-Engineers-Handbook-Volume-Two-Process-Control-and-Optimization/Liptak/p/book/9780849310812
14. Fagerlund AC and Chou DC. Sound transmission through a cylindrical pipe wall. Am Soc Mech Eng (Paper) 1980; 103(80).
15. Baumann HD and Singleton E. The IEC aerodynamic valve noise prediction standard revisited. Meas Control 2008; 41(5): 143–146.
16. International Electrotechnical Commission (IEC). IEC 60534-3: industrial process control valves - flow capacity - test procedures. IEC, 1997.
17. Karabasov SA. Understanding jet noise. Philos Trans R Soc A: Math Phys Eng Sci 2010; 368(1924): 3593–3608.
18. Instrument Society of America. ISA-RP75.23, considerations for evaluating control valve cavitation. Instrument Society of America, 1995.
19. Fenini L. Numerical modelling of flow-induced noise emitted by control devices. Phd. Thesis, Politecnico di Milano, 2019.
20. Mazzaro G. Rumore fluidodinamico in dispositivi di regolazione (Fluid-dynamic noise in control devices). Msc. Thesis, Politecnico di Milano, 2014.
21. Proudman I. The generation of noise by isotropic turbulence. Proc R Soc London Ser A Math Phys Sci 1952; 214(1116): 119–132.
22. Sarkar S and Hussaini M. Computation of the sound generated by isotropic turbulence. Proc R Soc London Ser A Math Phys Sci 1993; 94(1991): 218–280.
23. Mesbah M. Flow noise prediction using the stochastic noise generation and radiation approach. Phd. Thesis, KU Leuven, 2006.
24. Perini F, Zha K, Busch S, et al. Comparison of linear, non-linear and generalized RNG-based k-epsilon models for turbulent diesel engine flows. SAE Technical Paper 2017-01-0561, 2017.
25. Quaroni LN. Fluid-dynamic noise in control devices: a CFD approach. Msc. Thesis, Politecnico di Milano, 2020.