THE HIGHLY ENERGETIC EXPANSION OF SN 2010bh ASSOCIATED WITH GRB 100316D

Filomena Bufano1,2,3, Elena Pian3,4,5, Jesper Sollerman6, Stefano Benetti7, Giuliano Pignata2, Stefano Valenti7, Stefano Covino8, Paolo D’Avanzo8, Daniele Malesani9, Enrico Cappellaro7, Massimo Della Valle10,11, Johann Fynbo9, Jens Hjorth9, Paolo A. Mazzali7,12, Daniel E. Reichart13, Rhaana L. C. Starling14, Massimo Turatto3, Susanna D. Vergani14, Klas Wiersema14, Lorenzo Amati15, David Bersier16, Sergio Campana8, Zach Cano16, Alberto J. Castro-Tirado17, Guido Chincarini18, Valerio D’Elia19,20, Antonio de Ugarte Postigo9, Jinsong Deng21, Patrizia Ferrero22, Alexei V. Filippenko23, Paolo Goldoni24,25, Javier Gorosabel17, Jochen Greiner16, Francois Hammer27, Pall Jakobsson28, Lex Kaper29, Koji S. Kawabata30, Sylvio Klose31, Andrew J. Levan32, Keiichi Maeda33, Nicola Masetti34, Bo Milvang-Jensen9, Felix M. Mirabel23,35, Palle Møller36, Ken’ichi Nomoto33, Eliana Palazzi37, Silvia Piranomonte19, Ruben Salvaterra37, Giulia Stratta19, Gianpiero Tagliaferri8, Masaoi Tanaka33, Nial R. Tanvir14, and Ralph A. M. J. Wiess20

1 INAF-Osservatorio Astronomico di Catania, Via Santa Sofia, I-95123, Catania, Italy
2 Departamento de Ciencias Fisicas, Universidad Andres Bello, Av. Republica 252, Santiago, Chile
3 INAF-Osservatorio Astronomico di Trieste, Via G.B. Tiepolo 11, I-34143 Trieste, Italy
4 Scuola Normale Superiore di Pisa, Piazza dei Cavalieri 7, 56126 Pisa, Italy
5 INAF-Sezione di Pisa, Largo Pontecorvo 3, 56127 Pisa, Italy
6 The Oskar Klein Centre, Department of Astronomy, AlbaNova, SE-106 91 Stockholm, Sweden
7 INAF-Osservatorio Astronomico di Padova, Vicolo dell’Osservatorio 5, I-35122 Padova, Italy
8 Dark Cosmology Centre, Niels Bohr Institute, University of Copenhagen, Juliane Maries Vej 30, DK-2100 Copenhagen, Denmark
9 INAF-Osservatorio Astronomico di Brera, Via Emilio Bianchi 46, Merate I-23807, Italy
10 INAF-Osservatorio Astronomico di Capodimonte, Salita Moiariello, 16, I-8013 Napoli, Italy
11 Institute of Cosmology and Gravitation, University of Portsmouth, Portsmouth, UK
12 Max-Planck-Institut für Astrophysik, Karl-Schwarzschildstr. 1, D-85740 Garching, Germany
13 Department of Physics and Astronomy, University of North Carolina at Chapel Hill, Campus Box 3255, Chapel Hill, NC 27599-3255, USA
14 Department of Physics and Astronomy, University of Leicester, University Road, Leicester LE1 7RH, UK
15 INAF-Istituto di Astrofisica Spaziale e Fisica cosmica, Via Gobetti 101, I-40129 Bologna, Italy
16 Astrophysics Research Institute, Liverpool John Moores University, 2 Rodney Street, Liverpool L3 5UX, UK
17 Institutu de Astrofisica de Andalucia (IAA-CSIC), Glorieta de la Astronomia s/n, 18008 Granada, Spain
18 Dip. di Fisica G. Occhialini, Universitdi Milano Bicocca, P.zza della Scienza 3, Milano 20162, Italy
19 INAF-Osservatorio Astronomico di Roma, via di Frascati 33, 00040 Monte Porzio Catone, Rome, Italy
20 ASI-Science Data Center, Via Galileo Galilei, I-00044 Frascati, Italy
21 National Astronomical Observatories, CAS, 20A Datun Road, Chaoyang District, Beijing 100012, China
22 Instituto de Astrofisica de Canarias (IAC), 38200 La Laguna, Tenerife, Spain
23 Department of Astronomy, University of California, Berkeley, CA 94720-3411, USA
24 Laboratoire Astroparticule et Cosmologie, 10 rue A. Domon et L. Duquet, 75205 Paris Cedex 13, France
25 Service d’Astrophysique, DSM/IRFU/SAP, CEA-Saclay, 91191 Gif-sur-Yvette, France
26 Max-Planck-Institut für extraterrestrische Physik, Giessenbachstrasse 1, D-85740 Garching, Germany
27 GEPI-Observatoire de Paris Meudon, 5 Place Jules Janssen, F-92195 Meudon, France
28 Centre for Astrophysics and Cosmology, Science Institute, University of Iceland, Dunhagi 5, 107 Reykjavik, Iceland
29 Astronomical Institute Anton Pannekoek, University of Amsterdam, Science Park 904, 1098 XH Amsterdam, The Netherlands
30 Hiroshima Astrophysical Science Center, Hiroshima University, 1-3-1 Kagamiyama, Higashi-Hiroshima, Hiroshima 739-8526, Japan
31 Thuringer Landessternwarte Tautenburg, Sternwarte 5, D-07778 Tautenburg, Germany
32 Department of Physics, University of Warwick, Coventry CV4 7AL, UK
33 Institute for the Physics and Mathematics of the Universe, University of Tokyo, 5-1-5 Kashiwanoha, Kashiwa, Chiba 277-8583, Japan
34 INAF–Istituto di Astrofisica Spaziale e Fisica cosmica, Via Gobetti 101, I-40129 Bologna, Italy
35 IAE-CONICET-UBA, cb67, suc 28, Buenos Aires, Argentina
36 European Organization for Astronomical Research in the Southern Hemisphere (ESO), Karl-Schwarzschild-Str. 2, 85748 Garching, Germany
37 Dipartimento di Fisica e Matematica, Università dell’Insubria, via Valleggio 7, 22100 Como, Italy

ABSTRACT

We present the spectroscopic and photometric evolution of the nearby (z = 0.059) spectroscopically confirmed Type Ic supernova, SN 2010bh, associated with the soft, long-duration gamma-ray burst (X-ray flash) GRB 100316D. Intensive follow-up observations of SN 2010bh were performed at the ESO Very Large Telescope (VLT) using the X-shooter and FORS2 instruments. Thanks to the detailed temporal coverage and the extended wavelength range (3000–24800 Å), we obtained an unprecedentedly rich spectral sequence among the hypernovae, making SN 2010bh one of the best studied representatives of this SN class. We find that SN 2010bh has a more rapid rise to maximum brightness (8.0 ± 1.0 rest-frame days) and a fainter absolute peak luminosity (Lbol ≈ 3 × 1051 erg s−1) than previously observed SN events associated with GRBs. Our estimate of the ejected 56Ni mass is 0.12 ± 0.02 M⊙. From the broad spectral features, we measure expansion velocities up to 47,000 km s−1, higher than those of SNe 1998bw (GRB 980425) and 2006aj (GRB 060218). Helium absorption lines He I λ 5876 and He I 1.083 μm, blueshifted by ~20,000–30,000 km s−1 and ~28,000–38,000 km s−1, respectively, may be present in the optical spectra. However, the lack of coverage of the He I 2.058 μm line prevents us from confirming such identifications. The nebular spectrum, taken at ~186 days after the explosion, shows a broad but faint [O I] emission at 6340 Å. The light curve shape and photospheric expansion velocities of SN 2010bh suggest that we witnessed a highly energetic
1. INTRODUCTION

During the past decade, the link between long-duration gamma-ray bursts (GRBs) and Type Ic core-collapse supernovae (SNe; e.g., Filippenko 1997) has been firmly established; see Woosley & Bloom (2006) and Hjorth & Bloom (2011) for reviews. The first clear case occurred in 1998, when the luminous SN 1998bw, at $z = 0.0085$, was found spatially and temporally coincident with GRB 980425 (Galama et al.1998). The GRB–SN connection was supported in 2003 by two further associations between nearby GRBs and spectroscopically confirmed SNe: GRB 030329/SN 2003dh at redshift $z = 0.17$ (Hjorth et al.2003; Stanek et al.2003; Matheson et al.2003) and GRB 031203/SN 2003bw at $z = 0.11$ (Malesani et al.2004; Thomsen et al.2004; Gal-Yam et al.2004; Cobb et al.2004). The most recent case of a spectroscopic connection is GRB 060218/SN 2006aj ($z = 0.033$;Campana et al.2006; Pian et al.2006; Mirabal et al.2006; Modjaz et al.2006; Cobb et al.2006; Ferrero et al.2006). On average, SNe associated with classical GRBs appear to be more luminous at peak than SNe Ic not accompanied by GRBs, while SNe associated with X-ray flashes (XRFs) have maximum luminosities more similar to those of normal SNe Ic (see, e.g., Pian et al.2006; Pignata et al.2011; Drout et al.2011). However, SNe associated with both GRBs and XRFs exhibit broader features in their spectra, indicating unusually large expansion velocities. From the modeling of their light curves and spectra, very high explosion energies are inferred ($\sim 10^{52}$ erg, about 10 times higher than typical SNe), which earned them the name of hypernovae (HNe; Paczynski 1998; Iwamoto et al.1998). The GRB–SN connection has been best studied at low redshift ($z < 0.2$), where the clear, spectroscopically confirmed cases have been detected. Although GRBs at these low redshifts are rarely observed, the association between GRBs and SNe has been extended up to $z \sim 1$ (corresponding to a look-back time of about 60% of the age of the universe), in a number of GRB–SNe which have been identified through single-epoch spectra characterized by the presence of SN features (Lazzati et al.2001; Della Valle et al.2003, 2006, 2008; Soderberg et al.2005; Bersier et al.2006; Cobb et al.2010; Cano et al.2011a; Spera et al.2011; Berger et al.2011). The investigation of all confirmed GRB–SN associations is critical to understanding the nature of their progenitors and the mechanism by which powerful stripped-envelope SNe produce ultrarelativistic jets (e.g., Zhang et al.2003; Uzdensky & MacFadyen 2006; Mazzali et al.2008; Fryer et al.2009; Lyutikov 2011).

GRB 100316D (Stamatikos et al.2010) is a low-redshift event ($z = 0.059$; Vergani et al.2010; Starling et al.2011; see also Section 3.1), whose prompt emission is characterized by a very soft spectral peak, similar to that of XRFs (GRBs with energy peak at low frequency; Heise et al.2001), and a slowly decaying flux. A few days after its detection, an associated Type Ic SN was identified through the spectral features of the early optical counterpart: SN 2010bh (Chornock et al.2010b, 2010c; Wiersema et al.2010; Bufano et al.2010). Similar to the low-redshift X-ray flash GRB 060218, GRB 100316D had an unusually long duration ($T_{00} > 1300$ s) and a spectral-hardness evolution with a stable and soft spectral shape throughout the prompt and late-time emission (Starling et al.2011). The early X-ray spectrum of GRB 100316D, like that of GRB 060218 (Campana et al.2006), is best described by a power law plus a thermal component (Starling et al.2011; Fan et al.2011). The latter may be the signature of either the shock breakout following core collapse (Campana et al.2006; Waxman et al.2007) or additional radiation from the central engine (e.g., Ghisellini et al.2007; Li 2007; Chevalier & Fransson 2008).

We intensively monitored the optical and near-infrared (NIR) spectrophotometric evolution of SN 2010bh, starting $\sim 12$ hr after the Swift/BAT GRB trigger, which occurred on 2010 March 16 at 12:44:50 (Stamatikos et al.2010; UT dates are used throughout this paper), until about 2 months past the discovery, when solar constraints prevent further observations of the SN. To enable accurate host-galaxy subtraction, we reobserved the field 0.5–1 yr after the explosion. This campaign was the outcome of the coordination of various observing programs at the European Southern Observatory (ESO, Chile) Very Large Telescope (VLT)39 and at the Cerro Tololo Interamerican Observatory (CTIO, Chile). The spectral behavior of SN 2010bh from day 1.39 to day 21.2 has also been discussed by Chornock et al.(2010a) and photometry during the first three months after explosion has been presented by Cano et al.(2011b) and Olives et al.(2012). The larger wavelength range and improved phase coverage of our observations allow us to analyze the early phases in more detail and to push the investigation into the late evolutionary stages.

In Section 2, we present the data set and describe the data reduction methods, while in Section 3 we show the spectrophotometric evolution of SN 2010bh and compare it to that of the previously well studied GRB–SNe. In Section 4, we discuss the derived properties of the progenitor star and the explosion parameters, and we summarize our conclusions.

2. DATA ACQUISITION AND REDUCTION

2.1. Photometry

$UBVRI$ photometry of SN 2010bh was obtained with the FOcal Reducer and low dispersion Spectrograph (FORS2; field of view (FOV) 6.8 $\times$ 6.8; scale 0.25 pixel$^{-1}$; Appenzeller et al.1998) at the ESO VLT UT1 and with the 0.41 m Panchromatic Robotic Optical Monitoring and Polarimetry Telescopes (PROMPTs) 1 and 5 located at CTIO (FOV 10$^{\prime}$ $\times$ 10$^{\prime}$, 0.6 pixel$^{-1}$; Reichart et al.2005). The $R$-band images

---

39 VLT observations were taken within the GTO programs 084.D-0265 and 085.D-0701 (PI: S. Benetti) and 084.A-0260 and 085.A-0009 (PI: J. Fynbo) at UT2/X-shooter, and GO program 085.D-0243 (PI: E. Pian) at UT1/FORS2. SN 2010bh photometry on March 23 and 28 was obtained with GO program 084.D-0939 with UT1/FORS2 (PI: K. Wiersema). Observations were performed in ToO mode.

---

**Key words:** supernovae: general – supernovae: individual (SN 2010bh, GRB 100316D)

**Online-only material:** color figures
The Astrophysical Journal, 753:67 (13pp), 2012 July 1

Bufano et al.

Figure 1. Close-up view of SN 2010bh field from the R-band image taken with VLT/FORS2 on 2010 April 3 (scale in the lower-left corner). SN 2010bh and the sequence of local reference stars (Table 2) are reported.

Table 1
Journal of Late-epoch Template Observations

| UT             | JD (+2,400,000) | Phasea | Instr. | Bands |
|----------------|-----------------|--------|--------|-------|
| 2010 Sep 17    | 55456.8         | 184.8  | FORS2  | UBVRI |
| 2011 Jan 26    | 55587.5         | 315.5  | PROMPT5 | I     |
| 2011 Feb 2     | 55594.5         | 322.5  | PROMPT1 | VRI   |
| 2011 Feb 2     | 55594.5         | 322.5  | PROMPT5 | VR    |

Note. a Phases from Swift/BAT trigger (2010 March 16.53; Stamatikos et al. 2010).

from the X-shooter Acquisition Camera (FOV 1′47 × 1′47; 0′′173 pixel−1; D’Odorico et al. 2006) were also used to cover the early evolution. The data were reduced with standard techniques using IRAF40 tasks. Since the SN exploded in a region with a complex background, a template subtraction method, based on the ISIS package (Alard & Lupton 1998; Alard 2000), was applied to remove contamination from the host-galaxy light. As no pre-explosion observations were available of SN 2010bh, we used images obtained with VLT/FORS2 on September 17 (about 185 days past explosion; see Table 1), assuming that the SN flux contribution was negligible at this epoch (see Section 3). For PROMPT observations, template images were acquired on 2011 February 2, with the exception of the I band at PROMPT5, for which the template image was acquired on 2011 January 26 (see Table 1).

A point-spread-function (PSF) fitting method was applied to measure the SN magnitudes in the difference images. In particular, the PSF was derived from field stars measured on either the template or target image, whichever had the worst seeing. The kernel size was scaled according to the seeing to avoid truncation of the wings. We also performed aperture photometry on the subtracted images, obtaining very similar results. The uncertainties were estimated by means of artificial stars with the same magnitude as the SN; we first placed them close to the SN position (within few pixels) and then in the opposite side of the galaxy, where the background residuals were similar. The two approaches, intended to test for the effect of different background contributions, gave similar results. By observing several photometric standard fields, from Landolt (1992) for the U band and from Stetson (2000) for the BVRI filters, we obtained the color equations for each night and instrument, and used them to transform instrumental magnitudes to the standard photometric system. We calibrated the magnitudes of a local sequence of stars in the SN 2010bh field over four photometric nights (April 3, 5, 8 and 11) and used them to obtain the photometric zero points for the non-photometric nights (Figure 1 and Table 2). Because of the significant color term, we applied a calibration correction (S-correction) to the PROMPTs instrumental SN magnitudes to transform them into a standard photometric system following Pignata et al. (2008). Finally, a K-correction based on the nearly simultaneous spectra was applied to the observed BVRI magnitudes. For the U-band magnitudes, the signal-to-noise ratio (S/N) was too low to measure a reliable K-correction from the spectra. UBVR magnitudes of the SN are reported in Table 3 and plotted in Figure 2. We computed upper limit magnitudes (Table 3 and Figure 2) placing an artificial star at the SN position on the background-subtracted images and decreasing its magnitude down to the point of detectability over the background level. At template images epochs, limiting magnitudes were measured directly over the host-galaxy level, reported in Table 3 but not in Figure 2 because they do not set tight limits to the late-phase decline.

40 IRAF is distributed by the National Optical Astronomy Observatories, which are operated by the Association of Universities for Research in Astronomy, Inc., under contract with the National Science Foundation.
with the slit positioned along the north–south direction to minimize the host-galaxy contamination. For both instruments, the effects of atmospheric dispersion (Filippenko 1982) at high airmass have been reduced by using an atmospheric dispersion corrector. Simultaneous UV, VIS, and NIR spectra (~3000–24800 Å) were taken with X-shooter using slit widths of 1′′, 0′′.9, and 0′′.9 for each arm, respectively (D’Odorico

2.2. Spectroscopy

We followed the spectroscopic evolution of SN 2010bh with VLT/X-shooter (12 epochs) and VLT/FORS2 (8 epochs), as reported in Table 4. When possible, the spectra were acquired with the slit positioned along the north–south direction to

### Table 2

Optical Magnitudes of the Local Reference Stars in the Field of SN 2010bh

| Star ID | U       | B       | V       | R       | I       |
|---------|---------|---------|---------|---------|---------|
| 1       | 22.79 ± 0.06 | 21.74 ± 0.02 | 20.31 ± 0.03 | 19.43 ± 0.01 | 18.64 ± 0.02 |
| 2       | 19.88 ± 0.04 | 19.42 ± 0.02 | 18.57 ± 0.04 | 18.02 ± 0.01 | 17.51 ± 0.01 |
| 3       | 21.48 ± 0.09 | 21.57 ± 0.07 | 20.82 ± 0.04 | 20.35 ± 0.05 | 19.86 ± 0.03 |
| 4       | 18.84 ± 0.06 | 18.35 ± 0.02 | 17.55 ± 0.03 | 17.05 ± 0.01 | 16.57 ± 0.01 |
| 5       | 21.70 ± 0.10 | 21.86 ± 0.02 | 21.33 ± 0.03 | 21.33 ± 0.03 | 20.50 ± 0.02 |
| 6       | 21.24 ± 0.12 | 20.78 ± 0.02 | 19.98 ± 0.03 | 19.45 ± 0.01 | 18.98 ± 0.01 |
| 7       | 17.49 ± 0.07 | 17.49 ± 0.03 | 16.96 ± 0.02 | 16.60 ± 0.06 | 16.23 ± 0.07 |
| 8       | ...       | 22.58 ± 0.08 | 20.98 ± 0.03 | 20.02 ± 0.01 | 19.04 ± 0.02 |
| 9       | 18.30 ± 0.06 | 17.95 ± 0.02 | 17.18 ± 0.03 | 16.72 ± 0.03 | 16.25 ± 0.03 |
| 10      | ...       | 21.23 ± 0.08 | 19.78 ± 0.04 | 18.88 ± 0.01 | 18.14 ± 0.01 |

Note. No corrections have been applied to the reported magnitudes.

### Table 3

UBVRI Observed Magnitudes of SN 2010bh

| UT          | ID       | Phasea | U     | B     | V     | R     | I     | Instrument |
|-------------|----------|--------|-------|-------|-------|-------|-------|------------|
| 2010 Mar 17 | 55272.5  | 0.4    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 19 | 55274.5  | 2.4    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 20 | 55275.5  | 3.3    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 21 | 55276.5  | 4.2    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 24 | 55279.5  | 7.1    | ...   | ...   | ...   | ...   | ...   | FORS2      |
| 2010 Mar 25 | 55280.5  | 8.0    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 26 | 55281.5  | 8.9    | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 26 | 55281.7  | 9.1    | ...   | ...   | 19.66 ± 0.21 | ...   | ...   | PROMPT5*   |
| 2010 Mar 28 | 55283.5  | 10.8   | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 28 | 55283.5  | 10.8   | ...   | ...   | ...   | ...   | ...   | PROMPT5*   |
| 2010 Mar 28 | 55283.5  | 10.8   | ...   | ...   | ...   | ...   | ...   | PROMPT5*   |
| 2010 Mar 29 | 55284.5  | 11.8   | ...   | 21.05 ± 0.08 | ...   | ...   | ...   | FORS2      |
| 2010 Mar 29 | 55284.5  | 11.8   | ...   | ...   | 19.99 ± 0.15 | ...   | ...   | PROMPT5*   |
| 2010 Mar 30 | 55285.5  | 12.7   | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Mar 30 | 55285.5  | 12.7   | ...   | ...   | ...   | ...   | ...   | PROMPT5*   |
| 2010 Mar 31 | 55286.5  | 13.7   | ...   | ...   | 20.17 ± 0.19 | ...   | ...   | PROMPT5*   |
| 2010 Apr 1  | 55287.5  | 14.6   | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Apr 3  | 55289.5  | 16.5   | 20.85 ± 0.37 | 21.62 ± 0.06 | 20.38 ± 0.18 | ...   | ...   | FORS2      |
| 2010 Apr 5  | 55291.5  | 18.4   | 21.60 ± 0.21 | 21.99 ± 0.11 | 20.50 ± 0.13 | ...   | ...   | FORS2      |
| 2010 Apr 5  | 55291.5  | 18.4   | ...   | ...   | 20.49 ± 0.23 | ...   | ...   | PROMPT5*   |
| 2010 Apr 8  | 55294.5  | 21.2   | 22.14 ± 0.60 | 22.58 ± 0.07 | 20.83 ± 0.15 | ...   | ...   | FORS2      |
| 2010 Apr 11 | 55297.5  | 24.0   | 22.34 ± 0.51 | 22.64 ± 0.10 | 21.19 ± 0.10 | ...   | ...   | FORS2      |
| 2010 Apr 18 | 55304.5  | 30.6   | ...   | ...   | ...   | ...   | ...   | X-shooter  |
| 2010 Apr 24 | 55310.5  | 36.3   | ...   | ...   | 23.40 ± 0.07 | 22.02 ± 0.11 | ...   | ...   | FORS2      |
| 2010 Apr 28 | 55314.5  | 40.1   | ...   | ...   | ...   | 22.48 ± 0.09 | ...   | ...   | FORS2      |
| 2010 May 18 | 55334.5  | 59.0   | ...   | 23.4b  | 22.89 ± 0.13 | 22.13 ± 0.28 | ...   | ...   | FORS2      |
| 2010 Sep 17 | 55456.8  | 166.5  | 22.7b  | 21.7b  | 21.9b  | 21.4b  | 21.3b  | FORS2      |

Notes.

a Phases from Swift/BAT trigger (2010 March 16.53; Stamatíkos et al. 2010) in the host-galaxy rest frame. No corrections have been applied to the reported magnitudes, with exception of the (‘) S-correction for the PROMPT ones.

b Upper limit.
et al. 2006). We used a nodding throw along the slit (nodding lengths of 2″ and 4″) to obtain better sky subtraction. The data were reduced using version 0.9.4 of the ESO X-shooter pipeline (Goldoni et al. 2006) with the calibration frames (biases, darks, arc lamps, and flat fields) taken during daytime. After reducing the data using more advanced versions of the software, no relevant changes were found. With FORS2, we used the 300V grism (3300–9000 Å) and a slit width of 1″.

Both X-shooter and FORS2 spectra were extracted using standard IRAF tasks. Spectrophotometric and telluric standard-star exposures taken on the same night as the SN 2010bh observations were used to flux-calibrate the extracted spectra and to remove telluric absorption features. We checked the absolute flux calibration of the spectra by using the nearly simultaneous R-band magnitudes. Figure 5 shows the spectral sequence after correcting for both Galactic and host-galaxy reddening; both the wavelength scale and epochs are reported in the host-galaxy rest frame (see Sections 3.1 and 3.3). The most prominent emission lines of the host galaxy have been removed. Figure 6 is a zoom-in of the spectral sequence in the optical range. The three spectra taken in the nebular phase (2010 September 28 to October 1; see Table 4) have been combined to improve the S/N. The co-added spectrum is shown in Figure 9 (see Section 3.4).

### Table 4

| UT          | Phasea (days) | Telescope/Instrument | Arm/Grismb | Exptime (s) | Airmass |
|-------------|--------------|----------------------|-------------|-------------|---------|
| 2010 Mar 19.0 | 2.4          | VLT/X-shooter        | UV/VIS/NIR  | 2400/2400/2400 | 1.18    |
| 2010 Mar 20.0 | 3.3          | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.17    |
| 2010 Mar 21.0 | 4.2          | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.17    |
| 2010 Mar 23.0 | 6.1          | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.20    |
| 2010 Mar 24.0 | 7.1          | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.20    |
| 2010 Mar 25.0 | 8.0          | VLT/X-shooter        | UV/VIS/NIR  | 2400/2400/2400 | 1.18    |
| 2010 Mar 26.0 | 8.9          | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.18    |
| 2010 Mar 28.0 | 10.8         | VLT/X-shooter        | UV/VIS/NIR  | 2400/2400/2400 | 1.19    |
| 2010 Mar 30.0 | 12.7         | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.19    |
| 2010 Apr 01.0 | 14.6         | VLT/X-shooter        | UV/VIS/NIR  | 2400/2400/2400 | 1.21    |
| 2010 Apr 03.0 | 16.5         | VLT/FORS2            | 300V        | 1800        | 1.28    |
| 2010 Apr 05.0 | 18.4         | VLT/FORS2            | 300V        | 1800        | 1.22    |
| 2010 Apr 08.0 | 21.2         | VLT/FORS2            | 300V        | 1800        | 1.26    |
| 2010 Apr 11.0 | 24.0         | VLT/X-shooter        | UV/VIS/NIR  | 2400/2400/2400 | 1.20    |
| 2010 Apr 18.0 | 30.6         | VLT/X-shooter        | UV/VIS/NIR  | 2600/2600/3240 | 1.22    |
| 2010 Apr 24.0 | 36.3         | VLT/FORS2            | 300V        | 1800        | 1.34    |
| 2010 Apr 28.0 | 40.9         | VLT/FORS2            | 300V        | 3600        | 1.33    |
| 2010 Sep 26.0 | 195.8        | VLT/FORS2            | 300V        | 3600        | 1.60    |
| 2010 Sep 29.6 | 196.7        | VLT/FORS2            | 300V        | 7200        | 1.80    |
| 2010 Oct 01.7 | 198.8        | VLT/FORS2            | 300V        | 1260        | 1.47    |

**Notes.**

a Phases from Swift/BAT trigger (2010 March 16.53; Stamatikos et al. 2010) in the host-galaxy rest frame.
b X-shooter arm wavelength ranges are UV 3000–5600 Å, VIS 5500–10200 Å, and NIR 20200–24800 Å. FORS2 Grism 300V is 3300–9000 Å.

---

**Figure 2.** UBVI light curves of SN 2010bh. The abscissa represents the rest-frame time after the explosion, which is assumed to be coincident with the burst trigger (2010 March 16.53; Stamatikos et al. 2010). Magnitudes have not been corrected for Galactic and host-galaxy extinction. K-corrections have been applied to the BVRI magnitudes. FORS2 and X-shooter R-band photometry is reported with black and red solid circles, respectively. Open symbols are used for VRF magnitudes obtained with PROMPT. For clarity, the light curves are vertically displaced by the amount reported in the legend for each filter. (A color version of this figure is available in the online journal.)

SN 2010bh exploded at $\alpha = 07^h10^m30^s.53$ and $\delta = -56^\circ15'19.78''$ (J2000; Starling et al. 2011) in a bright anonymous galaxy. We measured the host-galaxy redshift by calculating the average shift of the central wavelengths of its strongest emission lines ([O II] 3727, Ne III λ3869, [O III] $\lambda\lambda4959, 5007$, Hβ Balmer lines, HeI $\lambda5876$, [O I] $\lambda6300$, [N II] $\lambda\lambda6584$, and [Si II] $\lambda\lambda6716, 6731$) in each of the 12 X-shooter spectra and correcting it for the radial component of Earth’s heliocentric motion. The weighted mean of the resulting heliocentric redshifts is $z = 0.0592 \pm 0.0001$. The high precision of the redshift estimate...
was possible thanks to the accuracy of the wavelength solution over the whole wavelength range of the X-shooter spectra (2 km s\(^{-1}\) for the UV and VIS arms). This value is in good agreement with the values presented in previous works (\(z \approx 0.059\), Vergani et al. 2010; \(z = 0.0591 \pm 0.0001\), Starling et al. 2011; \(z = 0.0593\), Chornock et al. 2010a). For a concordance cosmology (Hubble constant \(H_0 = 73\) km s\(^{-1}\) Mpc\(^{-1}\), \(\Omega_L = 0.73\), and \(\Omega_M = 0.27\)), we obtained a luminosity distance of about 254 Mpc (i.e., distance modulus \(\mu = 37.02\) mag).

We estimated the host-galaxy extinction by measuring the total equivalent width (EW) of the interstellar Na\(\text{I}\) D absorption doublet (\(\lambda\lambda 5890.0, 5895.9\)) with the assumption of a gas-to-dust ratio similar to the average ratio in our Galaxy. Measurements were performed on a spectrum obtained combining the almost featureless early-epoch X-shooter spectra (phases 2.4 days, 3.3 days, and 4.2 days, see Table 4). We found EW(\(\text{Na I} D\))\(_{\text{host}}\) = 0.59 ± 0.05 Å and EW(\(\text{Na I} D\))\(_{\text{milky Way}}\) = 0.30 ± 0.02 Å, giving a total EW(Na\(\text{I} D\))\(_{\text{host}}\) = 0.89 ± 0.07 Å (Figure 3). Applying the relation by Turatto et al. (2003), \(E(B - V) = 0.16 \times EW(\text{Na I} D)\)\(_{\text{host}}\) = 0.14 ± 0.01 mag, which is the value we adopt throughout this work. For the Milky Way extinction, we measured EW(\(\text{Na I} D\))\(_{\text{Milky Way}}\) = 0.40 ± 0.10 Å, while the second doublet component was not detectable (Figure 3). Assuming a flux ratio 2:1 between the two absorption lines, we obtained a total EW(Na\(\text{I} D\))\(_{\text{Milky Way}}\) = 0.60 ± 0.15 Å, implying \(E(B - V)_{\text{Milky Way}}\) = 0.10 ± 0.03 mag. This value is in agreement with that found by Schlegel et al. (1998), \(E(B - V)_{\text{Milky Way}}\) = 0.12 mag. We decided to adopt the latter because of the large uncertainty in our estimate of EW(Na\(\text{I} D\))\(_{\text{Milky Way}}\).

Recently, Poznanski et al. (2011) and Olivares et al. (2010) claimed that Na\(\text{I} D\) absorption may be a bad proxy for the extinction, especially if one uses low-resolution spectra where the two doublet lines cannot be resolved. Although we have a higher dispersion in the X-shooter spectra that allows us to separate the two components, we checked our result by estimating the reddening inside the host galaxy (along the line of sight) from the Balmer-line intensity ratios of the H\(\text{II}\) region coincident with the SN. First, we corrected both X-shooter and FORS2 spectra for the Milky Way extinction, then, assuming Case B recombination (\(T = 10^4\) K; Osterbrock 1989), we measured the H\(\alpha)/H\(\beta\) ratios from each spectrum. We obtained an average value of \(E(B - V)_{\text{host}}\) = 0.18 ± 0.06 mag, in agreement with that used in this work \(E(B - V)_{\text{host}}\) = 0.14 mag.

3.2. SN 2010bh Light Curves

Figure 2 illustrates the SN 2010bh light curves. Our R-band light curve traces well the early evolutionary stages; the SN...
Figure 5. SN 2010bh spectral evolution. The phase is given in rest-frame days after the explosion, assumed to be coincident with the GRB start time (2010 March 16.53; Stamatikos et al. 2010). The spectra are corrected for total (Milky Way + host-galaxy) reddening, shifted to the galaxy rest frame, vertically displaced, and rebinned for clarity. Dot-dashed vertical lines indicate the wavelengths of the minima in the Si\textsc{ii} and Ca\textsc{ii} absorption lines on the April 18 spectrum. The most prominent emission lines of the host galaxy have been removed and telluric band positions indicated.

reaches maximum light ($M_R \approx -18.5$ mag) at 8.0 ± 1.0 rest-frame days past the explosion, confirming the rise time independently found by Cano et al. (2011b) and Olivares et al. (2012). This is the steepest rise to maximum brightness ever found among both SNe associated with GRBs and broad-lined (BL) SNe for which explosion dates have been well constrained (e.g., SN 2002ap: $R_{\text{max}}$ at 12 days; Mazzali et al. 2007b; Foley et al. 2003; SN 2003jd: $R_{\text{max}}$ at ∼16 days; Valenti et al. 2008a; SN 2005nc: $R_{\text{max}}$ at ∼12 days; Della Valle et al. 2006). A decline of 0.056 ± 0.015 mag day$^{-1}$ is measured between 0 and 15 days after $R$-band maximum. Good sampling of the post-maximum phases was also obtained in the $UBVI$ bands (Figure 2). In Figure 4, we compare the $R$-band light curve of SN 2010bh with those of two previous well-sampled GRB–SNe: SN 1998bw (Galama et al. 1998; Patat et al. 2001) and SN 2006aj (Sollerman et al. 2006; Pian et al. 2006; Ferrero et al. 2006). The light curve of a more typical Type Ic SN (SN 1994I; Richmond et al. 1996) is also shown.

After maximum brightness, SN 2010bh and SN 1998bw have a similar behavior, but the decay rate of SN 2010bh between the last two $R$-band points corresponds to ∼0.03 mag day$^{-1}$ in the rest frame, to be compared with that of SN 1998bw (0.013 mag day$^{-1}$). Using the decline rates found by Patat et al. (2001) for SN 1998bw, we estimate the magnitudes of SN 2010bh at the epoch when the VLT subtraction images were acquired (+166.5 rest-frame days from maximum; see Table 1): $V \approx 25.0$, $R \approx 23.8$, and $I \approx 23.6$ mag. Considering this as an upper limit, if it was indeed the flux level of SN 2010bh, it would cause an oversubtraction and an underestimate of the SN fluxes in the $V$, $R$, and $I$ bands by less than 0.03 mag around maximum and 0.15 mag in the latest epochs. For each epoch, the corresponding inferred possible contamination by a residual SN flux has been included in the error estimate (Table 3).

SN 2010bh is less luminous than the other two GRB–SNe (Figure 4), which suggests a smaller amount of ejected $^{56}$Ni mass. Moreover, since the width of a light curve scales with the ratio between the total ejected mass $M_{ej}$ and the total explosion...
kinetic energy $E_k$ (Arnett 1982, 1996), the fast evolution of SN 2010bh likely reveals a relatively highly energetic explosion and/or a small $M_{ej}$. On the other hand, a highly asymmetric explosion may also result in a faster expansion in the polar direction, leading to a short diffusion time and a fast rise time (Maeda et al. 2006).

We note that our R-band photometry (neither corrected for Galactic or host extinction) at 0.5 days is $\sim$1 mag and $\sim$0.6 mag fainter than those of Cano et al. (2011b) and Olivares et al. (2012), respectively. This implies that we observe in our data the smooth rise in flux typical of an SN, and no evidence of the extra early component that they interpret as shock breakout. While we processed all raw data in a homogeneous way and consider this first flux point and its uncertainty formally correct, we caution that at these low-flux levels the X-Shooter acquisition camera imaging data may depend very critically on the assumed background.

### 3.3. Spectra in the Photospheric Phase

The spectral sequence of SN 2010bh (Figures 5 and 6) is unique among BL–SNe and HNe for its detailed temporal coverage and extended wavelength range (3000–24800 Å). At early epochs, the SED can be fit with a blackbody spectrum with $T_{bb} \approx 8500$ K. Thereafter, the continuum, shaped by broad bumps and absorptions, becomes redder with time because of expansion and cooling. The two main minima at $\sim$5500 Å and $\sim$7500 Å (Figure 6) can be identified with the blueshifted Si ii $\lambda$6355 and Ca ii NIR triplet $(g_f$-weighted line centroid $\lambda$8579) absorption lines, respectively. These lines are the most representative of the stratification of the expanding ejecta: their expansion velocities and evolution with time are shown in Figure 7. All velocities have been determined by fitting a Gaussian profile to the absorption features in the rest-frame spectra and measuring the blueshift of the minimum. The uncertainty that affects each line velocity has been taken to be equal to three times the standard deviation of the measured minimum positions. The velocity of Si ii $\lambda$6355 ranges from $\sim$36,000 km s$^{-1}$ at about seven days from the explosion to $\sim$25,500 km s$^{-1}$ at the last epoch. Ca ii velocities are systematically about 20% higher than those of Si ii. In Figure 7, we note that the velocity of the Si ii $\lambda$6355 line in SN 2010bh is higher than in SNe 1998bw and 2006aj, while it is similar to that of SN 2003dh, although with a shallower drop.

Considering its importance in constraining the nature and the evolutionary state of the progenitor star, we have searched for the spectroscopic signature of helium in our spectra. We observe weak absorption features in the optical and NIR that may be compatible with He i $\lambda$5876 and He i 1.083 μm blueshifted by $\sim$20,000–30,000 km s$^{-1}$ and $\sim$28,000–38,000 km s$^{-1}$, respectively (see Figure 6). The latter is in agreement with the velocities measured for Si ii and Ca ii. However, He i features may be blended with other species, like Na i in the optical and C i or Si i in the NIR (Mazzali & Lucy 1998; Millard et al. 1999; Sauer et al. 2006; Taubenberger et al. 2006). In particular, the contribution of C i cannot be ruled out. Indeed, by comparing the spectra of SN 2010bh to those of SNe 1998bw (Patat et al. 2001) and 2007gr (Valenti et al. 2008b) at similar epochs, we can identify the broad absorption at $\sim$1.6 μm with the C i...
Figure 8. Spectral comparison of SN 2010bh with other GRB–SNe (Patat et al. 2001; Mazzali et al. 2006a). Epochs are reported in rest-frame days after the explosion.

The λ16,890 line. Such absorption becomes more prominent starting eight days after explosion. A detection of the He\textsc{i} 2.058 μm line, typically not blended with other species, in the spectra of SN 2010bh is not possible, since the line, possibly blueshifted at any velocity up to 35,000 km s\(^{-1}\), would lie in the observed range 1.9–1.95 μm, which is heavily affected by telluric absorptions. Consequently, we cannot confirm the identification of He\textsc{i} λ5876 and He\textsc{i} 1.083 μm. Spectral modeling may help in recognizing the different ions contributing to the spectral line formation. This will be the scope of a future paper.

In Bufano et al. (2010), based on the spectrum taken on March 23, we reported the presence of a significant flux deficit in the range 4500–5500 Å. The flux density also seems low at wavelengths shorter than ∼3500 Å. From the spectral evolution (Figure 5), we can see that such deficits are seen only at this epoch. A careful analysis of the X-shooter spectrum has not identified any instrumental cause of these features. However, their time scale is too short to be explained physically, and therefore we will regard them as spurious.

In Figure 8, we compare the spectra of SN 2010bh with those of SNe 1998bw (Patat et al. 2001) and 2006aj (Mazzali et al. 2006a) at similar phases after explosion. At ∼4 days from the burst, both SNe 2006aj and 2010bh present a featureless spectrum, with the exception in the latter SN of a weak and broad (∼47,000 km s\(^{-1}\)) P-Cygni feature due to the Ca\textsc{ii} NIR triplet. This line becomes more prominent at later phases and displays a decreasing velocity (see also Figure 7). The Ca\textsc{ii} triplet velocity remains significantly higher than in SN 2006aj, for which Mazzali et al. (2006a) measured ∼25,000 km s\(^{-1}\) roughly constant with time. In SN 1998bw spectra, Patat et al. (2001) found that the main contribution to the absorptions at ∼7000 Å was given by O\textsc{i} (Figure 8), which is not obvious in our spectra of SN 2010bh. Absorptions at ∼3500 Å and ∼4500 Å in SN 2010bh spectra are likely due to Fe\textsc{ii} and Ti\textsc{ii}, as found for SN 2006aj through spectral modeling (Mazzali et al. 2006a).

3.4 Spectrum in the Nebular Phase

In the upper panel of Figure 9, we show the FORS2 nebular spectrum (∼186 days after explosion in the rest frame). At this time, no significant continuum flux contribution from the
Figure 9. Upper panel: FORS2 spectrum of SN 2010bh at \( \sim 186 \) rest-frame days after the explosion obtained by combining the spectra acquired in 2010 September and October (see Table 4). The blue line is the fit of the continuum we used to subtract the host-galaxy continuum flux contamination. Lower left panel: close-up view of the continuum-subtracted nebular spectrum in the wavelength interval 5500–7000 Å, centered on the expected wavelength of the \([\text{O} \, \text{I}]\) \( \lambda \lambda 6300, 6363 \) nebular emission lines. Lines from the host-galaxy \( \text{H} \, \text{II} \) region dominate. The broad emission at \( \sim 6300 \) Å is fitted with a Gaussian curve (green line). Lower right panel: the spectra of SN 1998bw at \( \sim 214 \) rest-frame days after explosion (red line; Patat et al. 2001) and SN 2006aj at 206 days (blue line; Mazzali et al. 2007a) are shown for comparison. The fluxes of SNe 1998bw and 2010bh have been normalized to that of SN 2006aj at the peak of the \([\text{O} \, \text{I}]\) line (the narrow \( \text{H} \, \text{II} \) region component, in the case of SN 2010bh). An additional rescaling of SN 1998bw has been done for clarity. (A color version of this figure is available in the online journal.)

supernova photosphere is expected. Therefore, since the SN exploded on a bright region of the host galaxy, we fit the spectral continuum with a polynomial function to obtain and subtract the background flux. The final continuum-subtracted nebular spectrum in the range 5500–7000 Å is plotted in the lower left panel of Figure 9. It shows the \([\text{O} \, \text{I}]\) narrow emission lines at 6300 Å and 6363 Å from the underlying galaxy region, and a broad but faint component, which, when fitted with a Gaussian function, peaks at 6340 Å with a total flux of \( 1.3 \times 10^{-16} \) erg cm\(^{-2}\) s\(^{-1}\).

From the comparison of SN 2010bh with SN 1998bw and SN 2006aj at similar rest-frame phases after the burst (214 and 206 days, respectively; Patat et al. 2001; Mazzali et al. 2007a; the lower right panel in Figure 9), we find that the \([\text{O} \, \text{I}]\) bump is very weak in SN 2010bh. The signal in the continuum-subtracted spectrum is too low to guarantee a secure measurement of the \([\text{O} \, \text{I}]\) abundance and to perform spectral modeling. However, taking into account the lack of strong evidence of \( \text{O} \, \text{I} \) lines in SN 2010bh spectra at early epochs, this could indicate a very small amount of ejected oxygen, and, consequently, a less massive progenitor than for SNe 1998bw and 2006aj. On the other hand, it could also be explained as a lower nebular

### Table 5

| SN          | \( E_k \) (10\(^{51}\) erg) | \( M_{\text{Ni}} \) (\( M_\odot \)) | \( M_{\text{ej}} \) (\( M_\odot \)) | \( E_k/M_{\text{ej}} \) (10\(^{51}\) erg \( M_\odot \)^{-1}) | Reference |
|-------------|-----------------|-----------------|-----------------|-----------------|----------------|
| SN 1998bw   | 50              | 0.38–0.48       | 11              | 4.5             | 2, 3          |
| SN 2003dh   | 40              | 0.25–0.45       | 8               | 5               | 4             |
| SN 2003bw   | 60              | 0.45–0.65       | 13              | 4.6             | 5             |
| SN 2006aj   | 2               | 0.21            | 2               | 1               | 6, 7          |
| SN 2010bh   | 9.7             | 0.12            | 3.2             | 3               | 1             |
| SN 2002ap   | 4               | 0.1             | 2.5             | 1.6             | 8             |
| SN 2003jd   | 7               | 0.36            | 3               | 2.3             | 9             |
| SN 2009bb   | 18              | 0.22            | 4.1             | 4.4             | 10            |

### References

(1) This paper; (2) Iwamoto et al. 1998; (3) Mazzali et al. 2001; (4) Mazzali et al. 2003; (5) Mazzali et al. 2006b; (6) Pian et al. 2006; (7) Mazzali et al. 2006a; (8) Mazzali et al. 2007b; (9) Valenti et al. 2008a; (10) Pignata et al. 2011.

flux, providing an indirect additional support for the \( M_{\text{Ni}}, M_{\text{ej}} \), and \( E_k \) values we found and discuss in the next section (see also Table 5). Indeed, considering that the energy input scales
roughly as $M_{\text{Ni}} \times (\tau_{\gamma} + 0.035)$, where $\tau_{\gamma}$ is the optical depth to radioactive gamma rays ($\tau_{\gamma} \approx 10^{3} M_{\text{Ni}}^{2} E_{k} r^{-2}$; see, e.g., Maeda et al. 2003) and 0.035 is the positron contribution, we obtain a late-time flux in SN 2010bh which is about a factor of $\sim 7$ and a factor of $\sim 2.5$ smaller than that in SN 1998bw and SN 2006aj, respectively (for the same distance and reddening).

3.5. Bolometric Light Curve

Since photometry in the individual bands is affected by possible spectral lines and their time evolution, it is important to construct a bolometric light curve to estimate reliably the SN physical parameters. As a first approximation, we obtained a quasi-bolometric $BVRI$ light curve using FORS2 photometry and the synthetic $BVRI$ magnitudes obtained from X-shooter spectra. To this aim, $BVRI$ magnitudes were first corrected for extinction and converted to flux density at the effective wavelength of the Johnson–Cousins filters. The SED was obtained from X-shooter spectra. To this aim, $BVRI$ magnitudes obtained from X-shooter spectra are equal to the integrated flux was converted into luminosity using the contribution from the $56\text{Ni}$ radioactivity and $56\text{Co}$—$56\text{Fe}$ decay (Sutherland & Wheeler 1984; Cappellaro et al. 1997). For a detailed description of the model see Valenti et al. (2008a). The bolometric light curve model suggests a total ejected mass of radioactive $56\text{Ni}$ of $M_{\text{Ni}} = 0.12 \pm 0.02 M_{\odot}$. The lack of measurements during the nebular phase prevents us from verifying this value through the radioactive tail.

Although a direct comparison with the quasi-bolometric curves created by Cano et al. (2011b) and Olivares et al. (2012) is not possible because of the difference in the wavelength ranges used to construct them, our $M_{\text{Ni}}$ estimate is in good agreement with that of Cano et al. (2011b) who found a $56\text{Ni}$ mass of $M_{\text{Ni}} = 0.10 \pm 0.01 M_{\odot}$. Olivares et al. (2012) derived a higher value ($M_{\text{Ni}} = 0.21 \pm 0.03 M_{\odot}$), likely because of the higher extinction correction.

4. DISCUSSION AND CONCLUSIONS

In order to obtain further information on the explosion and stellar progenitor, we compared the observed properties of SN 2010bh with those of SN 2006aj. We find that the SN 2010bh $R$-band light curve width was $\tau_{\text{peak},10bh} = (0.96 \pm 0.11) \times \tau_{\text{peak},06aj}$ by “stretching” its timescale in order to match the SN 2006aj light curve (see Perlmutter et al. 1997) and its photospheric expansion velocity $v_{\text{ph},10bh} = (1.74 \pm 0.05) \times v_{\text{ph},06aj}$ (assuming $\text{Si II} \lambda 6355$ as a good tracer, see, e.g., Valenti et al. 2008a).

Using the relations between $\tau_{\text{peak}}$ and $v_{\text{ph}}$ with the ejected mass $M_{\text{ej}}$ and the kinetic explosion energy $E_{k}$ ($\tau_{\text{peak}} \propto M_{\text{ej}}^{3/4} E_{k}^{-1/4}$; $v_{\text{ph}} \propto M_{\text{ej}}^{-1/2} E_{k}^{1/2}$; Arnett 1982, 1996), and the $M_{\text{ej}}$ and $E_{k}$ estimates of SN 2006aj found by Mazzali et al. (2006a), we derive $M_{\text{ej}} \approx (3.2 \pm 1.6) M_{\odot}$ and $E_{k} \approx (9.7 \pm 5.5) \times 10^{51}$ erg. From the analytical modeling of their pseudo-bolometric light curves, Cano et al. (2011b) and Olivares et al. (2012) found comparable ejected masses: $M_{\text{ej}} = 2.24 \pm 0.08 M_{\odot}$ and $M_{\text{ej}} = 2.6 \pm 0.2 M_{\odot}$, respectively. While the kinetic energy found by Cano et al. is not too dissimilar from ours ($E_{k} = (1.39 \pm 0.06) \times 10^{52}$ erg), the one derived by Olivares et al. is significantly larger, $E_{k} = (2.4 \pm 0.7) \times 10^{52}$ erg. These discrepancies are related to the different species used for the velocity measurements and to the uncertainties of the measurements themselves that are affected by line blending and by some arbitrariness in the choice of the line profiles. These problems are overcome by the use of a radiative transport model.

Although the photometric evolution of SN 2010bh was similar to that of SN 2006aj (i.e., similar light curve width), SN 2010bh had a higher $M_{\text{ej}}$ and $E_{k}$, explaining the faster expansion.
velocities measured from the spectra. This could suggest that spectra are more sensitive than light curves to possible effects of the viewing angle, in case of asymmetric explosion (a bipolar explosion is expected in the presence of a GRB; Piran 2004). Then we would expect that the weakest GRB (most off-axis) also has the lowest registered $E_{\gamma}/M_{\text{ej}}$ ratio. In Table 5, we report the $M_{\text{ej}}$ and $E_{\gamma}$ values found for previous GRB–SNe and other broad-lined SNe Ic, as well as the corresponding $E_{\gamma}/M_{\text{ej}}$ ratio, and thus plot the latter versus the relative ejected Nickel mass ($X_{\text{Ni}}$) (Figure 11). While SN 2010bh has an intermediate $E_{\gamma}/M_{\text{ej}}$ ratio, it lies on the low Nickel mass tail of the energetic Type Ic SN distribution (SN 2002ap, Mazzali et al. 2007b; SN 2003jd, Valenti et al. 2008a). The main reasons for such a wide variety among GRB–SNe cannot rely only on differences in the viewing angle, but must be intrinsic (e.g., explosion collimation, progenitor mass, etc.). Indeed, GRB–SNe have been supposed to come from different explosion scenarios (see Woosley & Bloom 2006 and references therein), where the core collapse of a massive progenitor star ($20-60 \msun$) leads to the formation of different central engines (a magnetar or a black hole). On the other hand, this heterogeneity does not have an obvious correspondence in the properties of the GRB. In Figure 12, the intrinsic peak energy is plotted as a function of the isotropic emitted energy (see, e.g., Amati et al. 2009), showing that GRB–SN events, including GRB 100316D, are consistent with the correlation in the $E_{\gamma,i}-E_{\text{iso}}$ plane, holding for all long GRBs (with the exception of GRB 980425). As noted by Starling et al. (2011), GRB 100316D has prompt gamma-ray spectral properties similar to GRB 060218.

The similarity between the light curves of SN 2010bh and SN 2006aj and between the observational characteristics of their associated GRBs suggests a common explosion mechanism for these two events. SN 2010bh would be produced by the core collapse of a relatively massive progenitor star ($20-25 \msun$), which leaves behind a magnetar, similar to SN 2006aj (Mazzali et al. 2006a). Indeed, by analyzing the spectral and temporal properties of the associated GRB 100316D, Fan et al. (2011) claimed that SN 2010bh was possibly powered by a magnetar with a spin period of $P \approx 10$ ms and a magnetic field $B \approx 3 \times 10^{15}$ G. In this picture, the magnetar rotational energy would be injected in the expanding remnant on a timescale set by the magnetic dipole radiation. Following Equation (2) of Kasen & Bildsten (2010), we would expect $t_{\text{d}} \approx 12$ hr; thus, even if a good fraction of the pulsar energy is converted into radiation, it will be lost by adiabatic expansion before escaping from the ejecta. Maeda et al. (2007) argued that in SN 2006aj the contribution from the magnetar to the light curve was likely negligible compared with the $^{56}\text{Ni}$ power, and this could be applicable in general to all magnetar-powered GRBs/XRFs.

We consider the detection at \~$12$ hr after the burst ($R \approx 21.4$ mag) as the contribution from the “cooling envelope” during the post-shock breakout phases (we may also have a non-thermal contribution from the afterglow at this phase). Following Chevalier & Fransson (2008), we estimate the progenitor radius: using their Equations (4) and (5) and $E_{\gamma}$ and $M_{\text{ej}}$ from our Table 5, we obtain the expected blackbody luminosity and temperature at 12 hr for different progenitor radii. Then, the expected blackbody spectrum was converted to the observed frame (assuming the SN 2010bh redshift and total color excess) and convolved with the $R$-band filter. The resulting magnitude was fainter than the observed one only in the case of a progenitor radius $R \lesssim 10^{11}$ cm. Even considering the $3\sigma$ upper limit flux, we would obtain a progenitor radius of the same order. This estimate is certainly rough, since it is based only on the single $R$-band image and uses simplified formulae (Chevalier & Fransson 2008), but it could provide support for a compact progenitor scenario and it is also consistent with the initial radius of $7 \times 10^{11}$ cm found by Olivares et al. (2012) analyzing the early X-ray-to-NIR emission.

On the other hand, we cannot exclude a scenario in which the outcome of GRB 100316D/SN 2010bh was a black hole, which could explain the small ejected mass as a consequence of the possible fall-back of ejecta onto the black hole. Recently, such small ejected masses have been inferred from the kinematics of black holes with $>10 \msun$ in our Galaxy, such as Cygnus X-1 (Mirabel & Rodrigues 2003; Gou et al. 2011), GRS 1915, and V404 Cyg (Mirabel 2011). However, in this case it may be difficult to accommodate the higher expansion velocities measured for SN 2010bh than those of previous HNe with a collapsar progenitor (e.g., SN 1998bw).

As anticipated, the high $v_{\text{ph}}$ may likely be explained as an effect of the explosion geometry. Good indicators of the explosion geometry are the nebular emission lines of Fe II (a blend near 5200 Å) and [O I] ($\lambda\lambda$6300,6363; Maeda et al. 2002, 2006; Mazzali et al. 2005), whose profiles can reveal the presence of asymmetry. No such information on the SN 2010bh explosion geometry can be deduced from its nebular spectrum because of the faintness of the emission lines.

We thank the ESO shift coordinators and night assistants for their excellent support during the observational campaign: A. Alvarez, T. Rivinius, T. Szejtli, T. Bensby, C. Ledoux, J. Smoker, C. Melo, F. J. Selman, S. Mieske, S. Steffl, P. Lynam, and V. D. Ivanov. We thank L. Koopmans for allowing us to activate our program during his scheduled observing time on 2010 March 18. F.B. is grateful to S. Taubenberger for fruitful discussion. F.B., S.B., E.C., S.V., and M. Turatto are supported by grant ASI-INAF I/009/10/0, and E. Pian by grant ASI-INAF I/088/06/0. Financial support from PRIN INAF 2009 is acknowledged. E. Pian acknowledges hospitality at the ESO HQs in Santiago, where part of this work was accomplished. G.P. acknowledges support by the Proyecto FONDECYT 11090421.
REFERENCES

Alard, C. 2000, A&A, 144, 363
Alard, C., & Lupton, R. H. 1998, ApJ, 503, 325
Amati, L., Frontera, F., & Guidorzi, C. 2009, A&A, 508, 173
Amati, L., Frontera, F., Tavani, M., et al. 2002, A&A, 390, 81
Appenzeller, I., Fricke, K., Fürting, W., et al. 1998, Messenger, 94, 1
Arnett, W. D. 1982, ApJ, 253, 785
Arnett, W. D. 1996, Space Rev., 78, 559
Bersier, D., Fruchter, A. S., Strolger, L.-G., et al. 2006, ApJ, 643, 284
Bufano, F., Benetti, S., Cappellaro, E., et al. 2010, CBET, 2227, 1
Campana, S., Mangano, V., Blustin, A. J., et al. 2006, Nature, 442, 1008
Cano, Z., Bersier, D., Guidorzi, C., et al. 2011a, MNRAS, 413, 669
Cappellaro, E., Mazzali, P. A., Benetti, S., et al. 1997, A&A, 328, 203
Chevalier, R. A., & Fransson, C. 2008, ApJ, 683, L135
Chornock, R., Berger, E., Levesque, E. M., et al. 2010c, CBET, 2228, 1
Cobb, B. E., Bailyn, C. D., van Dokkum, P. G., Buksz, M. M., & Bloom, J. S. 2004, ApJ, 608, L93
Cobb, B. E., Bailyn, C. D., van Dokkum, P. G., & Nataf, P. 2006, ApJ, 645, L131
Cobb, B. E., Bloom, J. S., Perley, D. A., et al. 2010, ApJ, 718, L150
Della Valle, M., Benetti, S., Mazzali, P. A., et al. 2008a, MNRAS, 383, 1485
Filippenko, A. V. 1997, ARA&A, 35, 309
Filippenko, A. V. 1982, PASP, 94, 715
Ferrero, P., Kann, D. A., Zeh, A., et al. 2006, A&A, 457, 857
Filippenko, A. V. 1998, 1999, ARA&A, 37, 309
Foley, R. J., Papenkova, M. S., Swift, B. J., et al. 2003, PASP, 115, 1220
Fryer, C. L., Brown, P. J., Bufano, F., et al. 2009, ApJ, 707, 193
Galama, T. J., Vreeswijk, P. M., van Paradijs, J., et al. 1998, Nature, 395, 670
Gal-Yam, A., Moon, D.-S., Fox, D. B., et al. 2004, ApJ, 609, L59
Ghisellini, G., Ghirlanda, G., & Tavecchio, F. 2007, MNRAS, 382, L77
Goldoni, P., Royer, F., Francois, P. et al. 2006, Proc. SPIE, 6269
Gou, L., Mcclintock, J. E., Reid, M. J., et al. 2011, ApJ, 742, 85
Hjorth, J., & Bloom, J. S. 2011, in Gamma-Ray Bursts, ed. C. Kouveliotou, R. A. M. J. Wijers, & S. E. Woosley (Cambridge: Cambridge Univ. Press) (arXiv:1104.2274)
Hjorth, J., Sollerman, J., Møller, P. et al. 2003, Nature, 423, 847
Iwamoto, K., Mazzali, P. A., Nomoto, K., et al. 1998, Nature, 395, 672
Iwamoto, K., Nomoto, K., Höflich, P., et al. 1994, ApJ, 437, L115
Kasen, D., & Bildsten, L. 2010, ApJ, 717, 245
Levesque, E. M., Berger, E., Soderberg, A. M., & Hjorth, J. (Berlin: Springer). 16
Lyutikov, M. 2011, MNRAS, 411, 2054
Maeda, K., Mazzali, P. A., Deng, J., et al. 2003, ApJ, 593, 931
Maeda, K., Mazzali, P. A., & Nomoto, K. 2006, ApJ, 645, 1331
Mazzali, P. A., Deng, J., Nomoto, K., et al. 2006a, Nature, 442, 1018
Mazzali, P. A., Deng, J., Pian, E., et al. 2006b, ApJ, 645, 1323
Mazzali, P. A., Deng, J., Tonimaga, N., et al. 2003, ApJ, 599, 394
Paczyński, B. 1998, ApJ, 494, L45
Paczynski, B. 1998, ApJ, 494, L45
Perlmutter, S., Gah, S., Goldhaber, G., et al. 1997, ApJ, 483, 565
Pignata, G., Benetti, S., Mazzali, P. A., et al. 2008, MNRAS, 388, 971
Pignata, G., Stritzinger, M., Soderberg, A., et al. 2011, ApJ, 728, 14
Piran, T. 2004, Rev. Mod. Phys., 76, 1143
Poonanski, D., Ganesalingam, M., Silverman, J. M., & Filippenko, A. V. 2011, MNRAS, 415, L81
Richardson, T. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 111, 327
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394
Richmond, W. M., van Dyk, S. D., Ho, W., et al. 1996, ApJ, 599, 394