Design and Performance Analysis of Proposed Single-Sided Linear Induction Motor used in Elevator

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ABSTRACT
In this paper, single-sided linear induction motor (SLIM) for driving the elevator system is designed. Differing from other motors, SLIM is simple in construction, less expensive, very suitable for linear application which is used from low speed to high speed application. Special machine adjustments and alignments are not necessary in SLIM because mechanical coupling and gears are not required. Thus, SLIM is superior to other linear and rotary motor. The single-sided linear induction motor (SLIM) design, performance equations and design procedure are developed and its performance is predicted by using equivalent circuit model. End effects and edges effects are neglected in this study. The performance of the SLIM for different value of mechanical air-gap are evaluated by using MATLAB. The effect of variation of such parameters on the performance of the machine is discussed.

Keywords: Linear Induction Motor, Single-Sided Linear Induction Motor (SLIM), Equivalent Circuit Model, Electrical Machine Design, Performance Evaluation

1. INTRODUCTION:
Linear induction motor (LIM), is basically an advanced types of motor that is use to obtain rectilinear motion instead of rotational motion as in ordinary conventional three phase induction motors. They may be obtained by “cutting” and “unrolling” the rotary induction machines to yield flat, single-sided topologies, where the cage secondary may be used as such or replaced by an aluminium sheet placed between two primaries to make the double-sided LIM. Linear motor potentially have unlimited applications. Linear induction motors (LIMs) alone have found application in the following general areas: conveyor systems, material handling and storage, people mover (Elevators), liquid metal pumping, machine tool operation, operation of sliding doors and low and high speed trains. There are different types of LIMs, among them, single-sided linear induction motors (SLIMs) are widely used in transportation system. In this paper, single-sided linear induction motor (SLIM) with short primary has been studied for the vertical conveying application because its main characteristic is the linear motion, which takes place without transformation mechanisms, increasing efficiency and the reliability of the system and also eliminating the need for large machine room on the roof. The SLIM has the following advantages comparing with the rotary induction motor (RIM): simple construction, direct electromagnetic thrust propulsion, safety and reliability, precise linear positioning, separate cooling, all electro-mechanical controlled systems used for an induction motors can be adopted for a SLIM without any bigger changes, economical and cheap maintenance.

2. STRUCTURE OF THE SINGLE-SIDED LINEAR INDUCTION MOTOR
The structure diagram of a short primary single-sided linear induction motor (SLIM) is shown in figure 1. The width of primary core, secondary yoke and back iron are different each other. Primary core is symmetrical to the secondary middle line. When the primary windings are excited with the three phase currents, a voltage is induced in the secondary. Thus, three axis forces are produced in the linear induction motor.
3. DESIGN PROCEDURE OF SINGLE-SIDED LINEAR INDUCTION MOTOR

The specifications of SLIM
- Target thrust, $F'_{s}$: 16000 N
- Rated velocity, $v_r$: 10 m/s
- Rated Slip, $s$: 10%
- Rated line voltage, $V_1$: 400 V
- Number of phase, $m$: 3phase
- Number of poles, $p$: 4poles
- Frequency, $f$: 50 Hz

Types of winding: Single Layer Winding

And, this machine is supposed to be applied in the elevator, achieving vertical transportation with ascending/rising speed $v_r$ and acceleration $a$ up to 10 m/s and 2 m/s$^2$ upwards, respectively. Therefore, the size of the cabin, total weight of cabin and necessary mechanical connection to it, and maximum allowable passenger and the average weight of each passenger are needed to know. All the necessary information are mentioned below

- Size of cabin, (height x length x width) $cabin = 2.5 \times 2 \times 1 m^3$
- Total weight of cabin and bearing, $m_{cabin} = 500$ kg
- Number of passenger in one cabin, $n_{p} = 5$
- Average weight of each passenger, $m_{passenger} = 75$ kg

3.1 Design of Primary (Stator)

Stator unit is designed according to the following procedure. First, assign the constant values

- Permeability of free space, $\mu_0 = 4\pi \times 10^{-7}$ H/m
- Volume resistivity of Copper, $\rho_{w} = 19.27 \times 10^6 \Omega m$
- Volume resistivity of Aluminum, $\rho_{r} = 28.85 \times 10^6 \Omega m$
- Stator current density, $J_1 = 6 A/mm^2$
- Maximum tooth flux density, $B_{max} = 1.6$ Tesla
- Maximum yoke flux density, $B_{ymax} = 1.3$ Tesla
- Coil span in electrical radians, $\theta_p = \pi$

Number of slot per pole per phase, $q_1 = 1$
Aluminum thickness, $d = 3$ mm
Width of stator, $W_s = 1000$ mm
Mechanical air gap, $g_m = 5$ mm

Continuously, to obtain the target thrust in a Single-Sided Linear Induction Motor, the following equations are used.

- Synchronous velocity, $v_s = \frac{v_r}{1-s}$ (1)
- Pole pitch, $\tau = \frac{v_s}{2f}$ (2)
- Slot pitch, $\lambda = \frac{\tau}{m_4}$ (3)
- Length of primary (Stator), $L_s = \tau p$ (4)
- $\tau \geq 3W_s + 3W_i$ (5)

In this design, the number of slot is 12 and single-layer winding $W_i = 1.5W_s$ (6)

And then, get the value tooth width and slot width shown in figure 2.

Number of turn per phase, $N = N_{pq}$ (7)

Where $N_i$ is the number of turn per phase and set the number of turn per slot $N_i$ to one and increment it by one until the target thrust is obtained.

Now, let assume the product of $\eta \cos \phi$ between 0 and 1 arbitrary.

And find, the value of stator current,

$$ I_i = \frac{F_s v_r}{3V_{w} \eta \cos \phi} $$ (8)

Area of copper wire, $A_s = \frac{I_i}{J_1}$ (9)

Total cross-sectional area of copper wire,$A_{w} = N_c A_w$ (10)
Cross-sectional area of slot, \( A_s = \frac{10}{7} N_s A_w \)  \( (11) \)

Stator slot height, \( h_s = \frac{A_w}{W_s} \)  \( (12) \)

Length of end connection, \( L_{ce} = \frac{\theta_p}{\tau} \)  \( (13) \)

Effective stator width, \( W_{est} = W_d + L_{ce} \)  \( (14) \)

Mean length of one turn of the stator winding per phase, \( L_{w1} = 2W_{est} \)  \( (15) \)

Length of copper wire per phase, \( L_w = N_l L_{w1} \)  \( (16) \)

Total length of copper wire, \( L_w = m L_w \)  \( (17) \)

After assuming the value of Aluminum thickness of conducting layer, \( d \), the magnetic air gap, \( g \), is calculated \( g_0 = g_{m} + d \)  \( (18) \)

And also find the equivalent stator width, \( W_{seq} = W_d + g_0 \)  \( (19) \)

Gamma for calculating carter’s coefficient, \( \gamma = \frac{4}{\pi} \left[ \frac{W_s}{2g_0} \cdot \arctan \left( \frac{W_s}{2g_0} \right) \right] - \ln \left( 1 + \left( \frac{W_s}{2g_0} \right)^2 \right) \)  \( (20) \)

Carter’s coefficient, \( k_c = \frac{\lambda_s}{\lambda_s \gamma g_0} \)  \( (21) \)

Effective air gap, \( g_e = k_c g_0 \)  \( (22) \)

The goodness factor, \( G = \frac{2\mu_\tau \pi^2}{\rho_p g_e} \)  \( (23) \)

Pitch factor, \( k_p = \sin \frac{\theta_p}{2} \)  \( (24) \)

Slot angle, \( \alpha = \frac{\pi}{m \theta_p} \)  \( (25) \)

Distribution factor, \( k_d = \frac{\sin \alpha}{2 q \sin \frac{\alpha}{2}} \)  \( (26) \)

Winding factor, \( k_w = k_p \times k_d \)  \( (27) \)

### 3.2 Equivalent Circuit Model

The equivalent parameters of SLIM can be determined using the per-phase equivalent circuit as shown in figure 3.

\[ I_1 \]
\[ R_1 \quad X_1 \]
\[ I_2 \]
\[ L_m \]
\[ V_i \]
\[ X_{se} \]
\[ R_{2/s} \]

Figure.3 Equivalent Circuit of Linear Induction Motor

Per-phase stator resistance, \( R_s = \frac{\rho_s L_w}{A_{st}} \)  \( (28) \)

Per-phase slot leakage reactance, \( X_{se} = \frac{2\mu_\tau \pi^2}{\rho_p g_e} \left[ \frac{\lambda_s}{1 + \frac{3}{p}} + \lambda_{d} \right] \frac{W_d}{d} \frac{L_{ce}}{N_l^2} \)  \( (29) \)

Magnetizing reactance per phase, \( X_m = \frac{24\mu_\tau \pi^2}{\rho_p g_e} k_c N_l^2 \frac{\tau}{\pi^2 g_e} \)  \( (31) \)

Using the equivalent circuit parameters from the above equations (28), (29), (31) and (32), and the circuit diagram shown in figure 3, the rated value of impedance can be calculated by

\[ Z = R_s + jX_s + \frac{R_s}{s} + jX_m \]

Power factor the design motor, \( \cos \phi = \frac{\Re(Z)}{|Z|} \)  \( (34) \)

The rated primary RMS phase current, \( I_1 = \frac{V}{|Z|} \)  \( (35) \)
Then magnitude of magnetizing current,
\[
I_m = \frac{R_s}{\sqrt{\left(\frac{R_s}{s}\right)^2 + X_m^2}} \times I_t
\]  
(36)

Also the magnitude of secondary phase current \( I_2 \) can be calculated from
\[
I_2 = \frac{X_m}{\sqrt{\left(\frac{R_s}{s}\right)^2 + X_m^2}} \times I_1
\]  
(37)

The SLIM input active power, \( P_i = mV_iI_t \cos \phi \)  
(38)

The output power, \( P_o = P_i - mI_1^2R_s - mI_2^2R_s \)  
(39)

And then efficiency is calculated by following equation
\[
\eta = \frac{P_o}{P_i} \times 100\% 
\]  
(40)

The electromagnetic force \( F \) produced by a machine is given by
\[
F = \frac{P_i}{V_r} 
\]  
(41)

### 3.3 Required Force Calculation

Resulting magnetomotive force (MMF),
\[
\theta_m = \frac{4\sqrt{2}mk_NI_m}{\mu_0} 
\]  
(42)

By mean of MMF, the peak value of the normal component of the magnetic flux density is given by
\[
B_{gmax} = \frac{\mu_0 \theta_m}{2g_0} 
\]  
(43)

Theoretically, the flux in the air gap is sinusoidal because of the sinusoidal voltage source. Thus, the average flux density \( B_{avg} \) can be gained, based on the relation with the peak value of that, i.e
\[
B_{avg} = \frac{2}{\pi} B_{gmax} 
\]  
(44)

The yoke of the primary core refer to the section at the top of the core showed in figure 2.
\[
h_y = \frac{B_{avg} \tau}{2B_{gmax}} 
\]  
(45)

Making use of \( L_s \), \( W_{st} \) and \( h_y \), the volume of the yoke is
\[
V_{yoke} = L_s W_{st} h_y 
\]  
(46)

In addition, the volume of one tooth of the primary core is
\[
V_{tooth} = W_{st} h_s 
\]  
(47)

Since the teeth have uniform size, the volume of the total teeth is derived as
\[
V_{teeth} = (mpq_i) V_{tooth} 
\]  
(48)

Where \( mpq_i \) is the number of slot in a primary core. So, the volume of the iron core of the primary core \( V_{iron} \) is
\[
V_{iron} = V_{yoke} + V_{teeth} 
\]  
(49)

The weight of the entire iron core, \( W_{iron} = \rho_1 V_{iron} \)  
(50)

The weight of copper wire, \( W_{c} = \rho_2 A t \)  
(51)

The weight of one primary unit \( W_{stator} \), consisting of iron core and copper wire, is easily obtained as
\[
W_{stator} = W_{iron} + W_{c} 
\]  
(52)

Number of primary unit, \( n_{stator} = \frac{h_{cabin}}{1.2L_s} \)  
(53)

And then, the total output thrust can be calculated as
\[
F = n_{stator} F_s 
\]  
(54)

Now checking the require force by Newton’s Second Law.

The mass of the whole rising system,
\[
m = n_{stator} m_{passenger} + n_{stator} W_{stator} + m_{cabin} 
\]  
(55)

The moving resistance of the system \( D \), consists of two components in this specific case, which are

Rolling resistance, \( D_r = m_c(c_1 + c_2 v_s) \)  
(56)

and aerodynamic resistance, \( D_a = \frac{1}{2} \rho v^2 A \)  
(57)

Where \( \rho \) is the air density 1.205kg/m³ and \( A \) is the top or bottom area of cabin 2m².
Total moving resistance is given by
\[ D = D_1 + D_a \]  
(58)

Now, making use of Newton’s Second Law of Motion, the force required to be produced by the propulsion system
\[ F_s = m (a + g) + D \]  
(59)

Where \( g \) is acceleration of gravity, \( 9.8 \text{m/s}^2 \).

Finally, \( F_s \geq F \) becomes a greatly important criterion to decide whether this machine design is satisfied or not.

### 3.4 Design of Secondary

The single-sided linear induction motor secondary (rotor) design contains conduction layer design and reaction plate design, it is illustrated in figure 4.

The secondary reaction plate design which can consist of either solid or laminated design. To improve performance, the reaction plate is coated with conduction sheet of either aluminium or copper. For standard operating, the reaction plate should not be any less than 6mm thick and the attached conducting sheet should not be any less than 3mm thick. The best thrust per size ratio is obtained.

\[ W_{se} = W_s + \frac{2\pi}{\pi} \]  
(60)

Where \( W_{se} \) is width of secondary and \( W_s \) is width of primary

### 4. DESIGN CALCULATION RESULTS OF SLIM

According to the design procedure in section 3, design calculation result of single-sided linear induction motor are mentioned with the following tables.

#### Table 1. Design of Primary

| Parameters                | Symbol | Values | Unit |
|---------------------------|--------|--------|------|
| Stator winding design     | Copper wire size | -     | 1 SWG |
|                          | Diameter of wire | -   | 7.62 mm |
|                          | Length of stator | L_s | 450 mm |
|                          | Width of stator | W_s | 1000 mm |
|                          | Slot width | W_s | 14.7 mm |
|                          | Tooth width | W_s | 22 mm |
|                          | Slot height | h_s | 32.73 mm |
|                          | Yoke height | h_s | 12.51 mm |

#### Table 2. Design of Secondary

| Parameters     | Symbol | Values | Unit |
|----------------|--------|--------|------|
| Length of secondary | L_se |     |      |
| Width of secondary | W_se | 1100 mm |
| Thick of conducting layer | d   | 3 mm  |
| Thick of reaction plate |         | 6 mm  |

The length of the secondary will be as long as the motion length. So, the length of secondary is not illustrated in table 2.

The design data sheet of electrical parameters of SLIM is presented in table 3. In the electrical parameters design, neglect the core losses.

#### Table 3. Design Output of Electrical Parameters

| Parameters                    | Symbol | Values | Unit |
|-------------------------------|--------|--------|------|
| Per-phase stator resistance   | R_1    | 0.00356 | Ω    |
| Per-phase stator slot leakage reactance | X_1 | 0.1371 | Ω    |
| Per-phase magnetizing reactance | X_m | 1.1795 | Ω    |
| Per-phase rotor resistance    | R_2    | 0.2055 | Ω    |
| Supply current                | I_1    | 201.605 | A    |
| Input active power            | P_i    | 62.854 | kW   |
| Output power                  | P_o    | 56.211 | kW   |
| Efficiency                    | η      | 0.89   | %    |
| Power factor                  | cosφ   | 0.45   | -    |

This motor is designed to move the total mass of 1643.5kg. It is needed 19.54kN output thrust with the rated velocity 10m/s. The outputs for the design motor are tabulated below table 4.

#### Table 4. Design Output of SLIM

| Parameters     | Symbol | Values | Unit |
|----------------|--------|--------|------|
| Total output thrust | F   | 22.5 kN |
| Velocity        | v    | 10 m/s |
5. PERFORMANCE CURVES OF SLIM
The input data used for SLIM design in MATLAB program was given in above section(3) along with the slot geometry. The performance characteristics of the SLIM are shown in following figures.

Also, output thrust and efficiency decrease when the design incorporates a large air gap. The goodness factor is inversely proportional to the air gap. Thus, it is clear that the air gap should be as small as is mechanically possible. The different performance values with varying air gap are shown in figure 7 and 8. When the air gap is changed, keeping all other parameters fixed, the efficiency slightly decreases with increasing air gap and the output thrust decreases as the air gap is increased.

6. PERFORMANCE EVALUATION OF SLIM BY CHANGING PARAMETER
The performance of the SLIM based on this particular design is evaluated by varying certain parameter like the mechanical air gap. Based on this evaluation, the best possible value for this parameter is selected as shown in the following sections.

6.1 Effect of Mechanical Air Gap on Performance
The length of the air gap plays the most critical role determining the characteristics of the machine. A large air gap requires a large magnetizing current and results in a smaller power factor. In the case of SLIM, exit-end zone losses increase with a larger air gap.

Table 5. Air Gap Effect on Thrust (Force) and Efficiency

| Air gap (mm) | Thrust (kN) | Efficiency (%) |
|-------------|-------------|----------------|
| 3           | 21.66       | 90             |
| 5           | 19.16       | 89.99          |
| 10          | 15.18       | 89.89          |

7. CONCLUSION
In this paper, the equivalent circuit has been derived to analyze the performance of the short primary SLIM. So, from the parametric analysis it can be concluded that the input parameter like the length of
the mechanical air gap plays a very important role in the performance parameters, thrust and efficiency. As the length of the mechanical air gap of the machine increases thrust and efficiency of the machine decrease. Hence, based on the target values of rotor velocity and thrust, this parameter should be chosen which gives the best possible thrust closest to the target value at a required frequency.

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