APPLY MACHINE LEARNING METHODS TO PREDICT FAILURE OF GLAUCOMA DRAINAGE

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Abstract

The purpose of this retrospective study is to measure machine learning models' ability to predict glaucoma drainage device failure based on demographic information and preoperative measurements. The medical records of 165 patients were used. Potential predictors included the patients' race, age, sex, preoperative intraocular pressure (IOP), preoperative visual acuity, number of IOP-lowering medications, and number and type of previous ophthalmic surgeries. Failure was defined as final IOP greater than 18 mm Hg, reduction in intraocular pressure less than 20% from baseline, or need for reoperation unrelated to normal implant maintenance. Five classifiers were compared: logistic regression, artificial neural network, random forest, decision tree, and support vector machine. Recursive feature elimination was used to shrink the number of predictors and grid search was used to choose hyperparameters. To prevent leakage, nested cross-validation was used throughout. With a small amount of data, the best classifier was logistic regression, but with more data, the best classifier was the random forest.

1. INTRODUCTION

Glaucoma Drainage Devices (GDDs) are typically utilized in the management of glaucoma refractory to maximal medical therapy or prior failed glaucoma surgery. The devices can be divided into two categories: non-valved (e.g. Molteno and Baerveldt) and valved (e.g. Ahmed). Non-valved GDDs have been shown to be more effective in lowering intraocular pressure (IOP) and have lower rates of reoperation than valved GDDs, but experience more frequent failure leading to dangerously low IOP or reduction of vision to the point of absolute blindness. However, there have been no studies directly comparing the two main types of non-valved GDDs despite their significantly different device profiles and implantation technique.

The accuracy of machine learning models in predicting GDD outcomes based on a minimal feature set provides a unique strategy to understand differences between these devices. Previous studies have predicted individual outcomes for other ophthalmic surgeries using machine learning and logistic regression. Achiron et al. used extreme gradient boosted decision forests to predict the efficacy (final VA/starting VA) of refractive surgery. Rohm et al. compared five algorithms to predict postoperative VA at 3 and 12 months in patients with neovascular age-related macular degeneration. Valdes-Mas et al. compared an artificial neural network with a decision tree to predict the occurrence of astigmatism and found the neural network superior. Mohammadi et al. used neural networks to predict the occurrence of posterior capsule opacification after phacoemulsification. Gupta et al. used linear regression to determine post-operative visual acuity based on patient demographics and pre-operative predictors. Koprowski et al. compared hundreds of artificial neural network topologies to predict corneal power after corneal refractive surgery. McNabb et al. used OCT (optical coherence tomography) to predict corneal power change after laser refractive surgery. Bowd et al. used Relevance Vector Machines to predict...
visual field progression in glaucoma patients based on SAP (standard automated perimetry) and CSLO (confocal scanning laser ophthalmoscope) measurements. More recently, Lee et al. used random forests and extremely randomized trees to predict glaucoma progression specifically in pediatric patients, also using SAP data. Similar to our own study, Baxter et al. used machine learning techniques (random forest, artificial neural network, and logistic regression) to predict surgical intervention for POAG (primary open-angle glaucoma) based on structured EHR data. They identified high blood pressure as a factor increasing the likelihood of surgical intervention, and several categories of ophthalmic and non-ophthalmic factors decreasing the likelihood of surgery. In contrast to their study, this one predicts implant failure instead of the need for surgical intervention, and includes more classifiers and types of glaucoma.

When comparing the Molteno and Baerveldt GDDs, demographic predictors included race, sex, and age at surgery. A total of seven clinical predictors were considered including:

**Implant Type:** Identified by type of implant (Molteno or Baerveldt) and implant plate surface area.

**VA (log MAR):** “Visual Acuity (Logarithm of the Minimum Angle of Resolution.)” A more reproducible visual acuity measurement often used in research. As Snellen visual acuity is more often collected in the clinic setting, conversion to log MAR allows easier statistical analysis.

**IOP:** Intraocular pressure. Elevated IOP is the major risk factor for development of glaucoma.

**Number of medications:** Include usage of beta-blockers, alpha-adrenergic agonists, prostaglandin analogs, or carbonic anhydrase inhibitors. The number of medications was calculated from patient records at each visit.

**Number of previous surgeries:** Glaucoma drainage implants are typically placed after less-invasive treatments fail but may incidentally be utilized following other ophthalmic surgeries (e.g. phacoemulsification of cataracts or retinal surgeries).

**Type of previous surgeries:** Include phacoemulsification or extracapsular cataract extraction (ECCE), trabeculectomy, pars plana vitrectomy, penetrating keratoplasty, Ex-PRESS shunt, iStent, or diode laser cyclodestructive laser cyclophotocoagulation (dCPC).

**Diagnosis:** Causes for glaucoma included open-angle, neovascular, uveitic, angle-closure, secondary to trauma, secondary to PKP, pseudoexfoliation, and combined mechanism.

## 2. DATA DESCRIPTION

### 2.1. Train Set

The train dataset contained 84 patients, of whom 64 had failure/no failure labels. Two additional patients were removed due to missing values.

Of 62 patients analyzed, 26 (41%) were determined to have device failure. The mean (± SD) follow-up time was 573±245.45 days, (range 133-1037 days). Patient samples were balanced between male and female. White race was three times more common than Black race and there was only one Asian patient (Tables 1 and 2). Implant failure was defined as having final IOP was greater than or equal to 18, IOP reduction of less than 20% from pre-operative levels, or repeat
surgery for glaucoma (this did not include in-clinic procedures that did not indicate failure of the device itself). By the last recorded appointment, 35% (22) of patients had a failing IOP and 19% (12) required additional surgery. No patients in this group experienced loss of light perception.

Table 1: Number of Participants by Race and Sex: Train Data

| Race | Male | Female | Total |
|------|------|--------|-------|
| Asian| 1    | 0      | 1     |
| Black| 8    | 8      | 16    |
| White| 24   | 21     | 45    |
| Total| 33   | 29     | 62    |

Table 2: Average Age at Surgery (Mean ± SD) by Race and Sex: Train Data

| Race | Male | Female | Average |
|------|------|--------|---------|
| Asian| 72±0 (1 total) | - | 72±0 (1 total) |
| Black| 61.9±9.7 (8 total) | 68.9±6.53 (8 total) | 65.4±8.1 (28 total) |
| White| 65.8±12.2 (24 total) | 69.4±6.53 (21 total) | 67.6±9.4 (58 total) |
| Average| 65.0±11.22 (33 total) | 69.2±6.53 (29 total) | 67.1±8.9 (62 total) |

A total of 42 patients received a Baerveldt GDD (67%) and 20 received a Molteno implant (27%). Forty-eight (77%) patients had surgery prior to placement of a GDD. Twelve patients (19%) required repeat surgery after initial placement of a GDD. Open-angle glaucoma was the most common underlying diagnosis (61%, n = 38) with combined mechanism (11%, n = 5) and chronic angle-closure (8%, n = 5) being less common. There were also individual patients with either neovascular, uveitic, traumatic, or pseudoexfoliation glaucoma. A diagnosis of "Other" was given for 8% of the patients, which indicated a singular diagnosis was not able to be determined from chart review.

2.2. Test Set

The dataset from which the test set was taken originally contained 122 patients, but after patients who also appeared in the train dataset or had missing values were removed, the final number of patients was 89 (Table 3).

The characteristics of the test set were similar to the train set. 39 of those patients (44%) were determined to have device failure. The mean (± SD) follow-up time was 626±284 days (range 107-1334 days). Patient samples were still relatively balanced between male and female, as in the train set. The racial makeup of this population was more balanced than the train set, with only twice as many white patients as black. The test set contained two Asian patients (Table 3).

Table 3. Number of Participants by Race and Sex: Test Data.

| Race | Male | Female | Total |
|------|------|--------|-------|
| Asian| 0    | 2      | 2     |
| Black| 13   | 15     | 28    |
| White| 25   | 33     | 58    |
| Other| 1    | 0      | 1     |
| Total| 39   | 50     | 89    |
Table 4. Average Age at Surgery (Mean ± SD) by race and sex: Test Data.

| Race | Male          | Female        | Average        |
|------|---------------|---------------|----------------|
| Asian| 67.1±9.4 (13 total) | 66.7±11.5 (15 total) | 66.9±10.6 (28 total) |
| Black| 67.1±13.2 (25 total) | 63.4±12.4 (33 total) | 65.0±12.9 (58 total) |
| White| 39.0±0.0 (1 total) | -             | 39.0±0.0 (1 total) |
| Other| 66.4±12.7 (39 total) | 64.5±12.27 (50 total) | 67.1±8.9 (62 total) |

The Average age at surgery (mean ± SD) by race and sex of test data is shown in Table 4. The clinical makeup of the test set was very similar to the train set. A total of 59 patients received a Baerveldt GDD (66%) and 20 received a Molteno GDD (22%). 62 patients (70%) had surgery prior to placement of a GDD. Open-angle glaucoma was the most common underlying diagnosis (57%) with traumatic (13%) glaucoma being less common.

3. METHODOLOGY

3.1. Overview

This study was approved by the Human Research Protection Office at Washington University School of Medicine in Saint Louis, MO and was in adherence to the Declaration of Helsinki. A retrospective chart review was performed for patients having undergone an uncomplicated Molteno or Baerveldt tube shunt surgery from July 01, 2013 to May 01, 2017.

All models in this study were validated using three-fold stratified cross validation, and all but the neural net were developed using recursive feature elimination and grid searches. To prevent data leakage, final validation, grid searching, and feature selection were performed in separate cross validation loops, as recommended by Krstajic et al.12 In the outer loop, the final model was tested; in the middle loop, the best hyper parameters were chosen; and in the inner loop, the best feature subsets were selected. Within each loop, three-fold stratified cross-validation was used. Scaling and centering for continuous variables was performed as part of the model fitting procedure. The Logistic Regression, SVM, Decision Tree, and Random Forest classifiers were implemented in Python using Scikit-Learn,13 and the Neural Network classifier was implemented in R using the caret package.14

3.2. Logistic Regression

Logistic regression, traditionally used for modeling, determines the class of each input variable by multiplying each feature by a constant, adding a bias term, and applying the logistic function. Any outcome above 0.5 is rounded to 1; any outcome below 0.5 is rounded to 0. When cross-validated on the train set, the optimal logistic regression classifier used L2 regularization and a C parameter of 1, and had an accuracy of 0.66±0.08 and a ROC (Receiver Operating Characteristic) of 0.67±0.08. Based on the coefficients of the logistic regression model listed in Table 3, Black race and initially taking beta-blockers is associated with implant failure.
Table 3: Feature Coefficients of Logistic Regression Classifier

| Feature                                      | Sign | Coefficient |
|----------------------------------------------|------|-------------|
| Black race                                   | +    | 0.83        |
| Initially taking Beta Blockers               | +    | 0.63        |
| White                                        | -    | 0.37        |
| Initially taking Carbonic Anhydrase          | -    | 0.36        |
| Baerveldt 350 mm2                            | -    | 0.28        |

3.3. Support Vector Machine (SVM)

A Support Vector Machine uses several data points (support vectors) to find the hyperplanes separating data classes that allow identification of a hyperplane giving the maximum margin. The best classifier had a cost parameter of 0. Table 4 shows the feature coefficients of SVM classifier.¹⁵
Table 4: Feature Coefficients of SVM Classifier

| Feature                                                        | Sign | Coefficient |
|----------------------------------------------------------------|------|-------------|
| Combined tube placement and phacoemulsification                | -    | 2           |
| Black race                                                     | +    | 1.41        |
| No previous surgeries                                          | -    | 1           |
| Baerveldt 350 mm²                                              | -    | 0.7         |
| Previous Phacoemulsification or ECCE                          | -    | 0.6         |
| Initially taking beta blockers                                 | +    | 0.59        |
| Primary Open-Angle Glaucoma                                    | +    | 0.49        |
| Previous Trabeculectomy                                        | -    | 0.36        |
| Initially taking carbonic anhydrase inhibitor                  | -    | 0.34        |
| Initial VA (logMAR)                                            | +    | 0.28        |

Like regression, race and initially taking beta-blockers have the most weight in causing implant failure. Primary Open-Angle Glaucoma show possibility of implant failure too. The SVM classifier had an accuracy of 0.61±0.03 and a ROC AUC of 0.62±0.03.

3.4. Decision Tree

A decision tree repeatedly picks a threshold to divide data until it places all data items in groups (mostly) of the same class. First, it finds the threshold for all features dividing data most cleanly. Then it chooses features producing the cleanest split and repeats the process separately for the data on each side of the split. The algorithm stops when the data divide into pure groups or when the number of points in each group is too small to divide further without overfitting\(^\text{15}\). We used a minimum of three data points per leaf node and the Gini impurity measure.
As described in Tables 5 and 6 and Figure 1, IOP and race are the most important factor in device failure. Combined GDD placement and phacoemulsification, age, and usage of the 245 mm2 Molteno GDD are other factors. Despite regression and SVM, initially taking beta-blockers does not appear in decision tree. The decision tree's overall accuracy was 0.5±0.05, and its ROC AUC was 0.45%±0.04. Low accuracy makes the efficiency of this method less than previous methods.
Table 6: Patient Groups Created Using Decision Tree

| Group Number | Decision | Count | Number of Females | Number of Males | Group Characteristics | Patient Features |
|--------------|----------|-------|-------------------|----------------|----------------------|------------------|
| 0            | Success  | 8     | 0                 | 0              | False                | Any ≤ 75.5      |
| 1            | Success  | 3     | 2                 | 1              | 0.4                  | False Any ≤ 75.5 |
| 2            | Failure  | 7     | 0                 | 7              | True False Any Any   | Any Any Any Any False |
| 3            | Success  | 4     | 2                 | 2              | 0.5                  | True False Any Any True  |
| 4            | Failure  | 4     | 0                 | 4              | True False Any Any   | Any Any Any Any False ≤ 0.44 Any |
| 5            | Success  | 4     | 2                 | 2              | 0.5                  | True True False Any Any Any Any True 0.44 Any |
| 6            | Failure  | 3     | 0                 | 3              | True True ≤ 73.5     | True Any Any Any Any |
| 7            | Success  | 4     | 3                 | 1              | 0.4                  | True True ≤ 73.5 True 21.0 ≤ x < 15.75 False Any Any Any Any |
| 8            | Failure  | 4     | 1                 | 3              | 0.4                  | True True ≤ 73.5 True 38.0 ≤ x < 21.0 False Any Any Any Any |
| 9            | Success  | 3     | 2                 | 1              | 0.4                  | True True ≤ 73.5 True > 38.0 False Any Any Any Any |
| 10           | Success  | 3     | 2                 | 1              | 0.4                  | True True ≤ 73.5 True > 15.75 True False Any Any Any Any |
| 11           | Success  | 4     | 4                 | 0              | 0.4                  | True True ≤ 73.5 True > 15.75 True True ≤ 3.5 Any Any |
| 12           | Success  | 3     | 2                 | 1              | 0.4                  | True True ≤ 73.5 True > 15.75 True True > 3.5 Any Any |
| 13           | Success  | 8     | 8                 | 0              | 0                   | True True ≤ 73.5 True Any Any Any Any Any Any |

3.5. Artificial Neural Network
Table 7: Importance of Features in Neural Network Classifier

| Feature                        | Importance | Feature                        | Importance |
|--------------------------------|------------|--------------------------------|------------|
| In-surgery Phacoemulsification | 7.413775   | No previous surgeries          | 3.987791   |
| Chronic angle-closure glaucoma  | 5.810634   | Open-Angle Glaucoma            | 3.899654   |
| Initially taking Beta Blockers  | 5.167789   | Previous Phaco or ECCE         | 3.894626   |
| Previous Express Shunt          | 5.097406   | Molteno 185 mm2                | 3.866003   |
| Baerveldt 350 mm2               | 4.649922   | Number of Previous Surgeries   | 3.782343   |
| Black                           | 4.559001   | Age at Surgery                 | 3.535026   |
| Combined Mechanism Glaucoma     | 4.380725   | Starting VAlogMAR              | 3.53318    |
| Molteno 245 mm2                 | 4.3772     | Initially taking Carbonic Anhydrase | 3.298634 |
| Initially taking Prostaglandins | 4.180157   | Previous Trabeculectomy        | 3.234256   |
| Starting Number of Medications  | 4.155031   | White                          | 2.994674   |
| Initially taking Alpha Agonists  | 4.114784   | Baerveldt 250 mm2              | 2.98814    |
| Male                            | 4.096719   | Initial IOP                    | 2.982531   |

A feed-forward artificial neural network imitates biological neural tissue using sequential layers of "neurons" that transform the underlying data and pass it on to the next layer. The root of a neural net is a perceptron: two or more inputs connected to a neuron, which then multiplies each input by a weight, adds an intercept, and applies an output function to the result. In a single-layer neural network, many perceptrons extract information from the underlying features, and a final neuron (or more for multiclass classification) combines the output from these nodes. A single-layer network with 25 hidden nodes (Fig. 2) was trained on the data. Combined GDD placement and phacoemulsification was indicated as the most important factor in failure. Chronic angle-closure glaucoma and initially taking beta-blockers were also associated with therapy failure, though to a lesser extent. Race with importance = 4.6 shows high effect on failure. The accuracy was 0.53±0.11 and the ROC AUC was 0.52±0.10.
3.6. Random Forest

A random forest averages the predictions of multiple decision trees trained on subsets of the data\textsuperscript{15}. Using ten decision trees, the algorithm identified age at surgery, initial IOP, and visual acuity as the most important factors determining device failure. Race and utilization of the larger Molteno device (245 mm\textsuperscript{2}) were associated with device failure, though to a lesser degree. The overall ROC AUC was 0.58±0.1, and the overall accuracy was 0.58±0.13.

4. CONCLUSION

Table 9: Accuracy and ROC score across all models. Red: high effect, Orange: low effect

| Methods           | Black race | Beta Blockers | Age       | Initial IOP | Molteno 245 mm\textsuperscript{2} | Cataract removal |
|-------------------|------------|---------------|-----------|-------------|---------------------------------|-----------------|
| Logistic Regression | Red        | Red           |           |             |                                 |                 |
| SVM               | Red        | Red           |           |             |                                 |                 |
| Random Forest     | Orange     | Red           |           |             |                                 |                 |
| Neural Network    | Orange     | Red           |           |             |                                 |                 |
| Decision Tree     | Orange     | Red           |           |             |                                 |                 |
Comparing results from different models identified Black race as the strongest factor associated with device failure. This finding aligns with existing research in the ophthalmology literature. Such failure rates are believed to be due to genetic differences in wound healing and proliferation of fibrovascular tissue. Use of topical beta-blockers pre-operatively was also associated with device failure. In treating glaucoma medically, prostaglandin analogs are often first-line with beta-blockers used second-line or as a reasonable alternative first-line agent. Alpha-agonists and carbonic anhydrase inhibitors are often added next, though they can cause intolerable allergic reactions and discomfort on instillation, respectively. These side effects can lead to drop intolerance and serve as an impetus for surgery. Therefore, it is perhaps not unsurprising that patients would be on beta-blockers when surgical intervention is needed as they are usually well-tolerated in those without respiratory problems. Nonetheless, beta-blockers association with implant failure in several models may be an area of further investigation. Placement of the larger Molteno GDD was associated with device failure, though this was a weaker association and found in weaker models. Again, this warrants further investigation given the devices function similarly. Lastly, age, increased IOP, and phacoemulsification at the time of GDD implantation were associated with failure in weaker models. Overall, the most accurate model was logistic regression, followed by a support vector machine model with a linear kernel. Our findings suggest machine learning techniques can accurately determine important features leading to failure of GDD implants from a large dataset of common clinical descriptors.

Table 11. Accuracy and ROC score across all models

| Methods          | Cross-Validation on Train | Test |          |          |
|------------------|---------------------------|------|----------|----------|
|                  | ROC AUC (mean ± SD)       | Accuracy (mean ± SD) | ROC AUC   | Accuracy |
| Logistic Regression | 0.67±0.08                | 0.66±0.08 | 0.64     | 0.58     |
| SVM              | 0.62±0.03                 | 0.61±0.03 | 0.68     | 0.64     |
| Random Forest    | 0.53±0.10                 | 0.58±0.13 | 0.85     | 0.74     |
| Neural Network   | 0.52±0.10                 | 0.53±0.11 | 0.55     | 0.57     |
| Decision Tree    | 0.45±0.04                 | 0.50±0.05 | 0.38     | 0.53     |

Based on Table 11, the logistic regression classifier had the best cross-validation performance on the train dataset. However, the random forest classifier benefited from training on all of the available train data, and had the highest performance in the test set.

REFERENCES

[1] D. L. Budenz et al., “Five-Year Treatment Outcomes in the Ahmed Baerveldt Comparison Study,” Ophthalmology, vol. 122, no. 2, pp. 308–316, Feb. 2015, doi: 10.1016/j.ophtha.2014.08.043.
[2] A. Achiron et al., “Predicting Refractive Surgery Outcome: Machine Learning Approach With Big Data,” J Refract Surg, vol. 33, no. 9, pp. 592–597, Sep. 2017, doi: 10.3928/1081597X-20170616-03.
[3] M. Rohm et al., “Predicting Visual Acuity by Using Machine Learning in Patients Treated for Neovascular Age-Related Macular Degeneration,” Ophthalmology, vol. 125, no. 7, pp. 1028–1036, Jul. 2018, doi: 10.1016/j.ophtha.2017.12.034.
[4] M. A. Valdes-Mas, J. D. Martin, M. J. Ruperez, C. Peris, and C. Monserrat, “Machine learning for predicting astigmatism in patients with keratoconus after intracorneal ring implantation,” in IEEE-EMBS International Conference on Biomedical and Health Informatics (BHI), Valencia, Spain, Jun. 2014, pp. 756–759, doi: 10.1109/BHI.2014.6864474.
[5] S.-F. Mohammadi et al., “Using artificial intelligence to predict the risk for posterior capsule opacification after phacoemulsification:,” Journal of Cataract & Refractive Surgery, vol. 38, no. 3, pp. 403–408, Mar. 2012, doi: 10.1016/j.jcrs.2011.09.036.

[6] M. Gupta, P. Gupta, P. K. Vaddavalli, and A. Fatima, “Predicting Post-operative Visual Acuity for LASIK Surgeries,” in Advances in Knowledge Discovery and Data Mining, vol. 9651, J. Bailey, L. Khan, T. Washio, G. Dobbie, J. Z. Huang, and R. Wang, Eds. Cham: Springer International Publishing, 2016, pp. 489–501.

[7] R. Koprowski, M. Lanza, and C. Irregolare, “Corneal power evaluation after myopic corneal refractive surgery using artificial neural networks,” BioMed EngOnLine, vol. 15, no. 1, p. 121, Dec. 2016, doi: 10.1186/s12938-016-0243-5.

[8] 8. R. P. McNabb, S. Farsi, S. S. Stinnett, J. A. Izatt, and A. N. Kuo, “Optical Coherence Tomography Accurately Measures Corneal Power Change from Laser Refractive Surgery,” Ophthalmology, vol. 122, no. 4, pp. 677–686, Apr. 2015, doi: 10.1016/j.ophtha.2014.10.003.

[9] 9. C. Bowd et al., “Predicting Glaucomatous Progression in Glaucoma Suspect Eyes Using Relevance Vector Machine Classifiers for Combined Structural and Functional Measurements,” Invest. Ophthalmol. Vis. Sci., vol. 53, no. 4, p. 2382, Apr. 2012, doi: 10.1167/iovs.11-7951.

[10] 10. J. Lee, Y. K. Kim, J. W. Jeoung, A. Ha, Y. W. Kim, and K. H. Park, “Machine learning classifiers-based prediction of normal-tension glaucoma progression in young myopic patients,” Jpn J Ophthalmol, vol. 64, no. 1, pp. 68–76, Jan. 2020, doi: 10.1007/s10384-019-00706-2.

[11] 11. S. L. Baxter, C. Marks, T.-T. Kuo, L. Ohno-Machado, and R. N. Weinreb, “Machine Learning-Based Predictive Modeling of Surgical Intervention in Glaucoma Using Systemic Data From Electronic Health Records,” American Journal of Ophthalmology, vol. 208, pp. 30–40, Dec. 2019, doi: 10.1016/j.ajo.2019.07.005.

[12] 12. D. Krstajic, L. J. Buturovic, D. E. Leahy, and S. Thomas, “Cross-validation pitfalls when selecting and assessing regression and classification models,” J Cheminform, vol. 6, no. 1, p. 10, Dec. 2014, doi: 10.1186/1758-2946-6-10.

[13] 13. F. Pedregosa et al., “Scikit-learn: Machine Learning in Python,” arXiv:1201.0490 [cs], Jun. 2018, Accessed: Nov. 22, 2020. [Online]. Available: http://arxiv.org/abs/1201.0490.

[14] 14. M. Kuhn, “Building Predictive Models in R Using the caret Package,” J. Stat. Soft., vol. 28, no. 5, 2008, doi: 10.18637/jss.v028.i05.

[15] 15. P.-N. Tan, M. Steinbach, and V. Kumar, Introduction to data mining, 1st ed. Boston: Pearson Addison Wesley, 2006.

[16] 16. “The advanced glaucoma intervention study (AGIS)*113. Comparison of treatment outcomes within race: 10-year results,” Ophthalmology, vol. 111, no. 4, pp. 651–664, Apr. 2004, doi: 10.1016/j.ophtha.2003.09.025.

[17] 17. D. Broadway, I. Grierson, and R. Hitchings, “Racial differences in the results of glaucoma filtration surgery: are racial differences in the conjunctival cell profile important?,” British Journal of Ophthalmology, vol. 78, no. 6, pp. 466–475, Jun. 1994, doi: 10.1136/bjo.78.6.466.

[18] 18. K. Inoue, “Managing adverse effects of glaucoma medications,” OPTH, p. 903, May 2014, doi: 10.2147/OPTH.S44708.