EVOLUTION OF THE IONIZING RADIATION BACKGROUND AND STAR FORMATION IN THE AFTERMATH OF COSMOLOGICAL REIONIZATION

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ABSTRACT

The temporal evolution of the ionizing UV background radiation field at high redshift provides a probe of the evolution of the early star formation rate. By comparing the observed levels of absorption in the highest redshift quasar spectra to the predictions of a hydrodynamic simulation, we determine the evolution of the photoionization rate (Γ) for neutral hydrogen in the intergalactic medium over the redshift range 4.9 ≤ z ≤ 6.1. After accounting for sampling variance, we infer a sharp increase in Γ from z ≈ 6.1 to z ≈ 5.8, probably implying reionization at this redshift. We find a decrease in Γ from z ≈ 5.6 to 5.2 at 3σ significance. This feature is a generic signature in the aftermath of reionization, entirely consistent with the cosmological reionization process being completed at z ≈ 6.1. This generic feature is a result of a significant change in the star formation rate subsequent to the cosmological reionization. There is an abrupt rise of the temperature of the intergalactic medium due to photoheating when it is reionized. This translates to a correspondingly sudden jump in the Jeans mass and a dramatic suppression of gas accretion onto the most abundant (subgalactic) halos at the epochs of interest. The star formation rate suffers a temporary setback in the aftermath of reionization, resulting in a temporary decrease in the amplitude of the ionizing radiation field.

On-line material: color figures

1. INTRODUCTION

The conventional wisdom based on the standard theory of structure formation says that the universe was reionized sometime in the redshift range z = 6–12 (Barkana & Loeb 2001). The relatively large uncertain range in redshift reflects our imperfect knowledge of the density fluctuations on small scales, star formation processes (e.g., efficiency, initial mass function, etc.) and feedback processes at high redshift. The latest observations of high-redshift quasars (e.g., Fan et al. 2001) are beginning to probe the lower bound of that window, and suggestions have been made that we may be witnessing the end phase of the cosmological reionization process at z ≈ 6, based solely on the appearance of a precipitous drop of transmitted flux at the rest-frame Lyα wavelength near z ≈ 6 in a single quasar spectrum (Becker et al. 2001, hereafter B01; Barkana 2002).

In this paper, we present an analysis of the ionizing background radiation field in the redshift range z = 4.9–6.1, using the absorption measurements in B01. Combining with previous data at lower redshift, we find that coming from high redshift, the ionizing radiation intensity displays a sharp rise at z ≈ 6, peaking at z = 5.6, a significant downturn from z ≈ 5.6 to 5.2 by a factor of ~0.6 and, subsequently, a consistent ascent from z = 5.0 to z = 2.4 by a factor of ~4. All these three features are consistent with a picture in which the cosmological reionization was near completion at z ≈ 6.

The first feature (i.e., the initial sharp rise) has been predicted by several authors previously (Cen & Ostriker 1993; Gnedin 2000a; Miralda-Escudé, Haehnelt, & Rees 2000). At present, the primary uncertainty for its determination observationally is the possibility that the high level of absorption in the single observed quasar at z = 6.28 is some kind of anomaly. (We show that it cannot be a simple statistical fluctuation in the absorption level.) Additional observed quasars at z ≈ 6.3 will be critical in this regard. Here we focus our attention on the relatively more robust measurements of the ionizing radiation field at z < 6 and show that the observed pause in the rise of the amplitude of the ionizing radiation field from z ≈ 5.6 to 5.0 could be due to suppression of star formation following reionization at z ≈ 6.

2. REIONIZATION AND THE EVOLUTION OF THE IONIZING BACKGROUND

Assuming the model in which the intergalactic medium (IGM) is almost completely ionized and the radiation background is uniform, we infer the evolution of the H ionization rate by requiring that the mean flux decrement in simulated spectra matches the observed values in the upper panel of Figure 2 of B01. This method was pioneered by Rauch et al. (1997) and extended in McDonald et al. (2000, 2001) and McDonald & Miralda-Escudé (2001). We apply the standard procedure using a hydrodynamic simulation of a flat universe dominated by a cosmological constant and cold dark matter (ΛCDM), with CDM density Ω_m = 0.3, Hubble parameter h = 0.67 (H_0 = 100 h km s^{-1}/Mpc), baryon density Ω_b = 0.035, power spectrum normalization σ_8 = 0.9, and large-scale primordial power spectrum slope n = 1. The simulation is Eulerian, with box size 25 h^{-1} Mpc divided into 768^3 cells (see R. Cen, J. P. Ostriker, J. X. Prochaska, & A. M. Wolfe, in preparation, for a more complete description). We use outputs from the simulation at z = 5 and z = 6, interpolating linearly between them when neces-
We then randomly choose many sets of five variation in a small redshift interval, except if the temperature changed overall amplitude of the points (not accounted for in the error bars), as can changing the cosmological parameters can cause coherent shifts in the

changing the temperature of the gas, however, none of these should cause variation in a small redshift interval, except if the temperature changed suddenly. [See the electronic edition of the Journal for a color version of this figure.]

Figure 1 shows the results for the evolution of $\Gamma_{-12}(z)$, the hydrogen ionization rate in units of $10^{-12}$ s$^{-1}$. The open squares are the old results from McDonald & Miralda-Escudé (2001). The filled squares are the new results, leaving out the highest redshift point, which we analyze differently than the others because the detected transmission is not significant, and the detector noise needs to be taken into account carefully. (This last point is represented by the triangle with 1 and 2 $\sigma$ upper limit bars.) The equally spaced bins in redshift are chosen to coincide with the majority of the points in Figure 2 of B01. As discussed below, the results have been rescaled to apply for the value of the baryon density favored by big bang nucleosynthesis, $\Omega_b h^2 = 0.02$ (Burles & Tytler 1998), instead of the value in the simulation, $\Omega_b h^2 = 0.0157$.

In detail, we determine a value of $\Gamma_{-12}$ and its error (which is dominated by sampling variance, except for the highest redshift point) for each B01 point using the simulation as follows. First, we construct the optical depth field, $\tau(v)$; i.e., the spectrum is $F(v) = \exp[-\tau(v)]$ along a large number of lines of sight through the simulation cube (256$^2$ for each face), normalized using an arbitrary value of $\Gamma_{-12}$ (i.e., $\tau \propto \Gamma_{-12}^{-1}$ for low-density gas in ionization equilibrium). We then randomly choose many sets of five 12.5 $h^{-1}$ Mpc long segments of spectrum, so that each set forms a combined spectrum of the length of our redshift bins, $\Delta z = 0.167$. (Note that this length depends slightly on cosmology and redshift; i.e., the spectra should be shorter by 26% at $z = 6$ in our model, corresponding to a 13% increase in the estimated error bars, which we account for in the plot.) For each 62.5 $h^{-1}$ Mpc chunk, we determine the value of $\Gamma_{-12}$ that produces the observed value of the mean transmitted flux fraction, $\bar{F}(v)$, which is $T(v)$ in the notation of B01. The mean of the $\Gamma_{-12}$ values for all the chunks is the inferred value of $\Gamma_{-12}$ for this observed data point, and the dispersion is the estimated error. Most redshift bins in B01 have several measured values of $\bar{F}$ in them, so we combine the inferred values of $\Gamma_{-12}$ within the bin using an error-weighted average, which takes into account fractional overlap when necessary. (Because of the overlapping points, our error bars are correlated in the sense that point-to-point differences are more significant than the error bars seem to indicate.)

To test that the treatment of 12.5 $h^{-1}$ Mpc segments as independent does not underestimate the sampling error by ignoring correlation along the lines of sight on larger scales, we repeat this procedure using 6.25 $h^{-1}$ Mpc segments and find almost identical error bars.

We now turn to the highest redshift point in B01. The given value and error are $F = 0.0038 \pm 0.0026$; however, B01 state that the sky subtraction has an uncertainty of order 1 $\sigma$, so we use $\sigma = 0.0052$ when interpreting this point. B01 also give the measured transmitted flux fraction in the region of the spectrum corresponding to Ly$\beta$ absorption by gas at this redshift, $F = -0.00024 \pm 0.0024$, and point out that the implied constraint on the Ly$\alpha$ optical depth is actually stronger than the direct one. We assume the same sky subtraction error for this point as for the Ly$\alpha$ region.

We start by analyzing the Ly$\alpha$ region. We use the method described above to create chunks of spectra of the appropriate length. For each value of $\Gamma_{-12}$, we compute $\bar{F}$ for many different chunks and compute the mean likelihood of producing $\bar{F} = 0.0038$ given the error $\sigma = 0.0052$. The relative likelihood function peaks at $\Gamma_{-12} = 0.059$ but does not decrease significantly for arbitrarily small $\Gamma_{-12}$. The likelihood has dropped by factors of 0.61 and 0.14 at $\Gamma_{-12} = 0.096$ and 0.135, respectively, so we call these the 1 and 2 $\sigma$ upper limits.

We analyze the Ly$\beta$ region in two ways. First, we repeat the above procedure assuming a constant factor 0.13 suppression of the continuum by Ly$\alpha$ absorption corresponding to gas at $z \approx 5$ (see the lowest redshift point in B01). The inferred 1 and 2 $\sigma$ upper limits on $\Gamma_{-12}$ are 0.032 and 0.056. These constraints are stronger than the ones from the Ly$\alpha$ region; however, they are not as realistic as possible because they ignore fluctuations in the Ly$\alpha$ absorption in the Ly$\beta$ region, which might either weaken the constraints by completely obscuring substantial portions of the Ly$\beta$ region or strengthen the constraints by providing regions of significantly less-than-average absorption where residual transmission through the Ly$\beta$ forest could be observed. We simulate this effect by creating Ly$\alpha$ absorption spectra to serve as the continua for the Ly$\beta$ region, using the $z = 5$ simulation output and our inferred value of $\Gamma_{-12}$ from the lowest redshift B01 point. This procedure results in essentially identical constraints to the assumption of a flat continuum: $\Gamma_{-12} < 0.032$ and 0.062 at 1 and 2 $\sigma$, respectively.

It may be possible to obtain even stronger constraints by using Ly$\gamma$, as suggested by B01 (X. Fan, 2001, private communication), or by considering the limits imposed by individual pixel values (D. Weinberg, 2001, private communication). However, if reionization is ongoing or just completed at $z = 6.1$, the detailed constraints on $\Gamma_{-12}$
obtained from any kind of analysis based on a simulation in which reionization happened much earlier probably are not very meaningful. (The value $\Gamma_{-12}$ is not well defined if the radiation background is inhomogeneous.) Our formal constraints on $\Gamma_{-12}$ near $z = 6$ should be taken simply as an indication that something dramatic is happening at this redshift, and we think it likely indicates the end of the cosmological reionization process.

The overall amplitude of our $\Gamma$ results (but not the evolution over a short-redshift interval) is sensitive to the cosmological model and gas temperature-density relation in the simulation, as one can see from the equation for optical depth at a point in space (i.e., ignoring peculiar velocities and thermal broadening) $\Delta = \rho_b/\rho_0$ and gas temperature $T$:

$$\tau \propto \frac{(\Omega_b h^2)^2 \Delta^2}{T_0^3 H(z)}$$

where $H(z)$ is the Hubble parameter at redshift $z [H(z) \simeq 100 h \Omega_m^{1/2}(1 + z)^{3/2}]$ at high $z$ in a $\Lambda$CDM universe. Sensitivity of the inferred value of $\Gamma$ to the power spectrum of density perturbations enters through the $\Delta^2$ term as well as the peculiar velocities, and additional sensitivity to temperature can arise from the thermal broadening. The effect of changing $\Omega_b h^2$ or $H(z)$ on the inferred value of $\Gamma$ is easy to correct for, but the effect of changing the temperature-density relation or the input power spectrum generally must be investigated by running additional simulations. We do this using approximate Hydro-PM simulations (hereafter HPM; Gnedin & Hui 1998), after checking that they give similar results to our fully hydrodynamic simulation (to $\sim 10\%$ in $\Gamma$) when performed using the same model and initial conditions. First, we analyze HPM simulations with a variety of different temperature-density relations and find that the thermal broadening is not very important to the derivation of $\Gamma$, so the dependence $\Gamma \propto T^{-0.7}$ is accurate (to $\sim 0.1\%$ in the power-law index), as long as the temperature is specified at the most relevant density for the transmission features that determine $\Gamma$, which we find to be $\Delta \sim 0.35$ (i.e., for a temperature-density relation $T = T_{0.35}(\Delta/0.35)^{-1}$, the inferred value of $\Gamma$ is independent of $\gamma - 1$). The temperature in our hydrodynamic simulation at this density is 5400 K, but in the aftermath of reionization, the temperature of the gas would be higher than this (e.g., Miralda-Escudé & Rees 1994), requiring a correction. The amplitude of the initial density fluctuations in our hydrodynamic simulation is higher by a factor of $\sim 1.5$ on the scale of the Ly$\alpha$ forest than the measurement of McDonald et al. (2000), which was independently confirmed by Croft et al. (2001). By varying the amplitude, $A$, in HPM simulations, we determine that $\Gamma \propto A^{-1.5}$ (roughly). The required ionizing background decreases when $A$ increases because the voids where transmission is observed become deeper (i.e., $\Delta$ becomes smaller). In the end, the corrections for power spectrum amplitude and temperature may roughly cancel (if we use $T \sim 10,000$ K), so the points in Figure 1 should be reasonably accurate; however, we emphasize that the temperature at this redshift is unknown, so significant uncertainty in $\Gamma$ remains.

The reader may be wondering at this point if the inferred decrease in $\Gamma_{-12}$ from $z \simeq 5.6$ to $z \simeq 5.2$ may be real. It appears to be a $3\sigma$ effect, and we think it could be real. The same trend is clearly visible to the eye in the bottom panel of Figure 2 of B01, once we consider that the value of their $\tau_{\text{eff}}$ is generally expected to increase with time. The signal is almost equally strong in the spectra of two different quasars. These two are at almost identical redshift, so a continuum-related effect might be the same in both; however, the observed $\sim 30\%$ increase in transmission fraction between $z \simeq 5.2$ and $z \simeq 5.6$ would require an increase $\lambda^{-4}$ in the quasar continuum. Finally, we have every reason to believe that our statistical error calculation is correct. The scatter in the inferred values of $\Gamma_{-12}$ for different B01 points in each redshift bin is in perfect agreement with our estimated error bars (e.g., $\chi^2 = 13.0$ for 10 degrees of freedom when we treat the three average values of $\Gamma_{-12}$ for the bins in the range $5.2 \leq z \leq 5.6$ as fitting parameters to be estimated from the individual points with error bars). Note that while it may look small to the eye, the fractional error on the $z = 5.25$ point is actually larger than the fractional errors on the following two points. Purely adiabatic temperature evolution $\propto (1 + z)^2$, which constitutes the steepest possible evolution in temperature (by ignoring the subsequent photoheating), instead of the essentially constant temperature in the simulation, would cause only a $7.5\%$ relative change in the $\Gamma$ values.

We think that the sharp rise of the radiation intensity at $z \simeq 6.1$ may be a fairly strong case for the completion of cosmological reionization at that epoch. However, note that a value of $\Gamma_{-12} \sim 0.03$ is not inconsistent in principle with a fully ionized intergalactic medium (IGM), since the neutral fraction near the mean density is still only $\sim 0.00007$. One is hampered by the high optical depth of an IGM that is still mostly ionized. It will be extremely valuable to look for additional signatures of cosmological reionization in its aftermath, where more flux is transmitted. We will therefore focus our discussion on the radiation field at $z \leq 6$.

### 3. Discussion

In the standard hierarchical structure formation theory, smaller structures began to form earlier than larger structures, simply because the amplitude of density fluctuations is a decreasing function of scale, and in linear theory, density fluctuations on all scales grow at the same rate. Under this general picture, the universe is conventionally thought to be reionized mostly by photons from stellar systems more massive than $10^8 M_\odot$, where atomic line cooling provides an efficient energy sink for gas that is collected and heated during gravitational collapse of halos (Haiman, Rees, & Loeb 1997; Gnedin & Ostriker 1997). Less massive systems, after having produced an insufficient amount of stars (Population III) to reionize the universe at an earlier epoch, can no longer form stars due to lack of cooling processes (Ostriker & Gnedin 1996; Haiman, Thoul, & Loeb 1996; Haiman, Rees, & Loeb 1997; Tegmark et al. 1997).

After reionization, the temperature of the intergalactic gas is raised to $\gtrsim 10^4$ K (Cen & Ostriker 1993; Miralda-Escudé & Rees 1994; Gnedin & Ostriker 1997). The subsequent effect of suppression of gas accretion onto small halos has been noted by many authors (Elstathiu 1992; Thoul & Weinberg 1996; Quinn, Katz, & Efstathiou 1996; Kepner, Babul, & Spergel 1997; Navarro & Steinmetz 1997; Kitayama & Ikeuchi 2000; Gnedin 2000b). The extent of this effect somewhat varies among the studies, and it is clear that our current treatment of the reionization process is far from ideal. Obviously, an adequate study would require simulations that include an accurate treatment of three-
dimensional radiative transfer processes and have high enough spatial and mass resolution. We do not have simulations of this caliber at present and attempt to make only a semiquantitative calculation to illustrate a consequence of reionization on star formation and the background radiation field, which we believe captures a primary feature of this process in a simple and intuitive fashion.

The accretion process of IGM gas onto halos is complex. However, the relatively simple physical state of the IGM gas makes a simple calculation physically relevant. Ignoring subsequent photoheating, impulsively photoheated IGM gas basically cools down adiabatically (Hui & Gnedin 1997); other cooling mechanisms involving atomic processes are unimportant until the gas reaches a sufficiently high density, such as that inside the virial radius of a halo. Thus, the evolution of IGM gas before virialization is adiabatic. If an IGM gas element reaches the virial radius of a halo, its temperature would be

\[ T_{\text{IGM}} = 1.5 \times 10^4 \left[ \frac{\left(1 + z\right)}{1.7} \right]^2 \left( \frac{\rho_c}{\langle \rho_{\text{gas}} \rangle} \right)^{2/3} \text{ K}, \]  

(2)

where \( \rho_c \approx 70 \langle \rho_{\text{gas}} \rangle \) is the density of a gas element at the virial radius of a halo, and \( \langle \rho_{\text{gas}} \rangle \) is the mean gas density at the time in question. This is the lower limit on the temperature of the IGM gas element when it reaches the virial radius of a halo, since there may be additional shock heating. We assume that the IGM is initially photoheated to \( 1.5 \times 10^4 \text{ K} \) at \( z = 6 \). If \( T_{\text{IGM}} \) is greater than the virial temperature of a halo, then the gas element would not be able to accrete onto the halo. Figure 2 shows the virial temperature \( T_v \) of a halo with virial mass equal to the nonlinear mass \( M_{\text{nl}} \) and \( T_{\text{IGM}} \) as a function of redshift. The nonlinear mass \( M_{\text{nl}} \) is the mass within a top-hat window at which the linear rms density fluctuation is unity.

The assumption of instantaneous reionization is just for the sake of plotting convenience and is not required to make our point. In a real universe, the reionization phase is complicated and is thought to progress on a timescale of a Hubble time, during which the mean (volume-weighted) radiation field builds up slowly to a value of approximately \( 10^{-24} \text{ ergs cm}^{-2} \text{ H}^{-1} \text{ s}^{-1} \text{ sr}^{-1} \) at Lyman limit, followed by a brief phase in which the majority of the baryons are ionized and a sudden jump in the amplitude of the mean radiation field intensity at Lyman limit to \( 10^{-22} \text{ ergs cm}^{-2} \text{ H}^{-1} \text{ s}^{-1} \text{ sr}^{-1} \) occurs within a redshift interval of a fraction of unity (Miralda-Escudé et al. 2000; Gnedin 2000a). We simply call this epoch of a sudden rise in radiation field the reionization epoch, marking the completion of the reionization process.

We see in Figure 2 that gas is able to accrete onto halos with virial temperatures \( T_v = 20-3 \times 10^4 \text{ K} \) or virial masses \( M_v \leq 5 \times 10^9 \text{ M}_\odot \) prior to \( z \approx 6 \). Stars formed inside halos with virial temperatures \( T_v = (1-3) \times 10^4 \text{ K} \) or virial masses \( M_v = 10^8-5 \times 10^8 \text{ M}_\odot \) are presumably primarily responsible for producing most of the ionizing photons immediately prior to \( z \approx 6 \), where atomic line cooling provides an efficient cooling process. Right after reionization, there is a dramatic inversion of the situation from \( z \approx 6 \) to \( z \approx 4.5 \), where \( T_{\text{IGM}} \) surpasses the virial temperature of typical halos. Such a switch has some interesting consequences: gas accretion onto the most abundant halos (about the nonlinear mass) is suddenly suppressed, and thus, star formation may be brought to a halt in typical halos. (Larger halos with higher virial temperature may still be able to form stars with a somewhat reduced rate due to the same effect.) Below \( z \approx 4.5 \), nonlinear mass again becomes larger than the Jeans mass and gas is once again capable of accreting onto typical halos with mass \( \geq 4 \times 10^9 \text{ M}_\odot \), and the star formation rate bounces back. We note that the cosmological model adopted may not be correct in fine details and is used only to illustrate the process. Therefore, the exact crossing redshift of the two curves at \( z = 4.5 \) should not be taken at its face value but rather as a generic feature. Just as a side note, the temperature of the IGM will be shock heated to higher temperatures at lower redshift (\( z \leq 2 \)) when longer waves break, which will cause the dashed curve in Figure 2 to turn back up again.

Let us now relate the star formation rate to the ionizing background radiation field. Our treatment is intended to be simple, but we think it contains the essence of the relevant physical processes. For gas immersed in a metagalactic ionizing radiation background, locally hydrogen photoionization is balanced by hydrogen recombination (to levels \( n = 2 \) or higher),

\[ \Gamma n_{\text{H}_1} = n_{\text{H}_1} \mu n_e \alpha(T), \]

(3)

where \( \Gamma \) is the photoionization rate (see Fig. 1); \( n_{\text{H}_1} \), \( n_{\text{H}_1} \mu \), and \( n_e \) are the neutral hydrogen, ionized hydrogen, and electron number densities, respectively; and \( \alpha(T) \) is the hydrogen recombination rate. Averaging spatially both sides of equation (1) gives

\[ \langle n_{\text{H}_1} \rangle = \frac{C \langle n_{\text{H}_1} \rangle^2 \alpha(T)}{\Gamma}, \]

(4)
where $C$ is the clumping factor of all gas participating in receiving ionizing photons (i.e., excluding gas in optically shielded regions). For simplicity, we have assumed that the gas is composed entirely of hydrogen. Since the neutral hydrogen fraction is much less than unity, we have simply replaced both the ionized hydrogen and electron number densities by the total hydrogen number density $n_H$. The mean free path of an ionizing photon in comoving length units is then

$$\lambda = \frac{1 + z}{\langle n_H \rangle} = \frac{(1 + z)}{C(z)} \frac{\Gamma(1 + z)}{C(z)} \frac{\sigma_H}{\sigma_H}, \quad (5)$$

where $\sigma_H$ is the hydrogen photoionization cross section. Using $\alpha = 4 \times 10^{-13}$ cm$^3$ s$^{-1}$, $\Gamma = 1.5 \times 10^{-13}$ s$^{-1}$ (see Fig. 1), and $\sigma_H = 2 \times 10^{-18}$ cm$^2$, we obtain $\lambda$ in comoving megaparsecs:

$$\lambda = 74 C(z)^{-1} \left( \frac{\Omega_b h^2}{0.02} \right)^{-2} \left( \frac{1 + z}{7} \right)^{-5} \text{comoving Mpc.} \quad (6)$$

Evidently, at $z \sim 6$, the mean free path of an ionizing photon is much smaller than the Hubble radius, and radiative processes may be treated locally by ignoring cosmological effects. But the mean free path is much greater than the typical separation between ionizing sources ($\sim 1$ comoving Mpc). In this case, we may relate the mean comoving specific emissivity of ionizing radiation $\epsilon_\nu$ (in units of ergs s$^{-1}$ Hz$^{-1}$ comoving cm$^3$) to the mean ionizing radiation intensity $J_\nu$ (in units of ergs s$^{-1}$ Hz$^{-1}$ sr$^{-1}$ cm$^{-2}$) by

$$J_\nu = \frac{\epsilon_\nu (1 + z)^2}{4\pi} = 8.9 \times 10^{26} C(z)^{-1} \left( \frac{\Omega_b h^2}{0.02} \right)^{-2} \left( \frac{1 + z}{7} \right)^{-3}. \quad (7)$$

The evolution of $C(z) \equiv 1 + \langle \delta^2 \rangle$ is yet undetermined. However, simple estimates may be made to gauge the range of variation. In the linear regime $\langle \delta^2 \rangle \ll 1$ we have $C(z) \propto (1 + z)\beta$, and in the extreme nonlinear regime $C(z) \propto (\delta^2) \propto (1 + z)^{-6}$; the actual situation is likely to be between these two limiting cases, since the recombination rate is most likely dominated by regions that are neither static nor linear. Let us for the moment parameterize $C(z) \propto (1 + z)^\beta$ with $-6 \leq \beta \leq 0$. We use the simulation outputs at $z = 5, 6$ to compute $C$ (recombination rate weighted, since the temperature for ionized regions varies) and find $\beta = -3.5$. Inserting $C(z)$ into equation (5) yields

$$J_\nu \propto \epsilon_\nu (1 + z)^{-3 - \beta}. \quad (8)$$

Clearly, in order for $J_\nu$ to increase with redshift, as indicated by observations in the redshift range $z = 5.2$--5.6 as shown in Figure 1, the comoving specific emissivity or comoving star formation rate has to increase with redshift. Taking the values shown in Figure 1 in the range $z = 5.6$--5.2, we obtain $J_\nu \propto (1 + z)^{0.8 \pm 0.4}$. (This fit used the third through fifth filled squares in Fig. 1. We obtain a flatter slope, $5.3 \pm 2.1$, with an acceptable $\chi^2$, if we add the second point at $z \simeq 5.1$.) This requires a decrease in star formation rate from $z = 5.6$ to $z = 5.2$ as $e \propto (1 + z)^{1.2 \pm 0.4 - \beta} \propto (1 + z)^{0.8 \pm 0.4}$ (for $\beta = -3.5 \pm 1.0$ determined from the simulation with a roughly estimated error, which reflects both uncertainties on cosmological models and uncertainties on the reionization process). Our analysis is in qualitative agreement with Barkana & Loeb (2000), who pointed out that the decrease in star formation subsequent to cosmological reionization may be detectable in the evolution of number counts of faint galaxies by Next Generation Space Telescope (NGST). It may be that we have detected this signature in the evolution $J_\nu$ or $\Gamma$.

4. CONCLUSIONS

In hierarchical structure formation theory, the evolution of the metagalactic ionizing radiation background may be characterized by five distinct phases: (1) From $z \sim 15$--20 to $z_n$ (which marks the end of reionization), the radiation field builds up slowly before individual ionizing H II regions overlap (preoverlap period; Gnedin 2000a). (2) In a brief period up to $z_n$, the majority of baryons are ionized in a short timescale and the radiation field jumps up by about 2 to 3 orders of magnitude, completing the reionization process (reionization epoch). (3) From $z_n$ to $z_{\text{jeans}}$, the radiation field pulls back significantly due to a decrease in the star formation rate as a result of reionization. We call this the aftermath of reionization. (4) From $z_{\text{jeans}}$ to $z_{\text{peak}} \sim 1$--2, the radiation field rises steadily with contributions from both stars in larger galaxies and quasars; and (5) From $z_{\text{peak}} \sim 1$--2 to $z = 0$, the radiation field drops off sharply due to the combined effect of the decreasing star/quasar formation rate and cosmological effects. Consistent with theoretical calculations, observations by McDonald & Miralda-Escudé (2001) and those shown in Figure 1 of this paper have confirmed phase 4 and observations by Shull et al. 1999 have confirmed phase 5.

In this paper we have interpreted the absorption in the spectra of the latest high-redshift quasars in the redshift range $z = 4.9$--6.1, searching for salient features pertaining to the reionization epoch (phase 2, above) and the aftermath of reionization (phase 3, above). Quite intriguingly, we appear to be seeing the aftermath of reionization and the end of the reionization epoch in these spectra, both of which seem to point to a cosmological reionization redshift of $z_n \sim 6$. Specifically, a predicted decrease of star formation rate in the aftermath of the reionization is indicated by the observations. While a few more high-redshift quasars are required to check that the complete absorption at $z = 6.1$ is not some kind of anomaly (e.g., a rare leftover neutral patch in an almost completely ionized universe), it appears that our conclusion with regard to the aftermath of reionization is more secure due to its independence of any single spectrum. It is still very urgent to enlarge the observational data sets to greatly firm up the conclusion and sharpen up the rate of evolution. If confirmed by future observations, this may be an indication that our current understanding of galaxy formation is approximately valid up to redshift $z \sim 6$. Furthermore, as suggested by Barkana & Loeb (2000), it will be important to independently detect this aftermath of reionization signature in the evolution of number counts of faint galaxies by NGST.

Since we appear to be observing the period directly after reionization, it becomes more important to perform dedicated simulations that achieve reionization at the appropriate redshift $z \sim 6$. This paper should be understood as an attempt to guide that effort by making some preliminary comparisons between data and an existing simulation.
in which reionization occurred somewhat earlier. Such future simulations are quite demanding because not only are high resolutions required, but also an accurate treatment of three-dimensional radiative transfer must be implemented.

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