RESEARCH ARTICLE

Simple, biologically-constrained CA1 pyramidal cell models using an intact, whole hippocampus context [version 2; peer review: 2 approved]

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Abstract

The hippocampus is a heavily studied brain structure due to its involvement in learning and memory. Detailed models of excitatory, pyramidal cells in hippocampus have been developed using a range of experimental data. These models have been used to help us understand, for example, the effects of synaptic integration and voltage gated channel densities and distributions on cellular responses. However, these cellular outputs need to be considered from the perspective of the networks in which they are embedded. Using modeling approaches, if cellular representations are too detailed, it quickly becomes computationally unwieldy to explore large network simulations. Thus, simple models are preferable, but at the same time they need to have a clear, experimental basis so as to allow physiologically based understandings to emerge. In this article, we describe the development of simple models of CA1 pyramidal cells, as derived in a well-defined experimental context of an intact, whole hippocampus preparation expressing population oscillations. These models are based on the intrinsic properties and frequency-current profiles of CA1 pyramidal cells, and can be used to build, fully examine, and analyze large networks.

Keywords

pyramidal cells, neuroscience, patch clamps

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Introduction

Networks of excitatory and inhibitory neurons are essential components constituting the functional structures of our brains. Dysfunction is thought to occur when inappropriate excitation-inhibition balances occur. From a modeling perspective, these balances are determined by the choice of parameters in the equations representing neurons and networks. Mathematical models of neurons and networks are developed so that they can be used to determine the mechanisms underlying brain functions. However, it is difficult to assess whether the mechanisms determined from mathematical models actually occur biologically. Furthermore, it is well known that cellular models used in building network models affect and can dictate the network output. To address this recognized difficulty, we are developing models that are based on well-defined experimental contexts in which both cellular and population (network) aspects can be characterized. That is, we are building network models that are constrained based on experimental preparations in which intracellular and extracellular recordings (local field potentials) are simultaneously recorded, as described in other studies. Using such models, we aim to determine, predict and test mechanisms underlying population network output occurring in biological systems.

Here we use a well-defined experimental context of an in vitro intact, whole hippocampus preparation in which spontaneous population theta and theta-gamma rhythms are expressed. Access to many cellular details is possible in vitro, and with a physiologically relevant output of theta and theta-gamma rhythms, a reasonable and functional scenario is also present. We have previously developed models of CA1 fast-spiking inhibitory cells in the same experimental context, and used them to show that model inhibitory networks of these fast-spiking cells exhibit sharp transitions between random and coherent firings at high frequencies (>90 Hz) when connectivity constraints were imposed. In this article, we present the result of CA1 pyramidal cell models developed in the same context of this in vitro whole hippocampus preparation. Similar to our previous cellular model developments, the models presented here are biologically-based at the cellular level, but do not have a biophysical representation in terms of conductance-based model representations. These CA1 models use a simple two variable mathematical formulation based on Izhikevich and they include rebound firing and adaptation characteristics. Using these simple, yet biologically-based models, we are building and examining large network models that are aligned with the biology. Subsequent analyses of these large network models could determine the mechanisms by which particular cellular characteristics critically contribute to the population activities observed in our experimental context.

Methods

Experimental data

Animals. Three mice (two female, post-natal day 20–29) were used. We used transgenic mice that expressed a fluorescent protein, tdTomato, under the control of the PV promoter. PV-Cre homozygote mice (strain name: B6;129P2-Pvalbtm1(cre)Arbr/J, stock number: 008069, Jackson Laboratory) were mated with a reporter line, Ai9 homozygote mice (strain name: B6;129S6-Gt(Rosa)26Sortm9(CAG-tD amato)Bltm1/J, stock number: 007905, Jackson Laboratory) to generate PV-tdTomato mice. The mouse lines are on genetic backgrounds that are mixtures of C57BL/6 and a type of 129 mice; PV-Cre mice are C57BL/6;129P2 and Ai9 mice are C57BL/6;129S6. Mice were bred in-house at the Douglas animal facility and kept in standard laboratory cages with standard bedding and environmental enrichment. They were housed in a temperature-controlled room with a 12:12 hours dark/light cycle with food and water provided ad libitum. All animals were treated according to protocols and guidelines approved by McGill University and the Canadian Council of Animal Care (CCAC). Ethical approval was obtained to conduct this study (approval number: 2010-5827). The authors note that the use of scissors to decapitate mice at that age without administering anesthesia (which could have altered synaptic transmission) was approved by the CCAC.

Intact hippocampal preparation. The acute preparation containing the whole hippocampus was obtained from PV-tdTomato mice according to a previously described protocol. Briefly, after decapitation using scissors, the brain was quickly removed from the skull and placed in ice-cold high-sucrose solution, containing (in mM) 252 sucrose, 24 NaHCO3, 10 glucose, 3 KCl, 2 MgCl2, 1.25 NaH2PO4 and 1 CaCl2 (pH 7.3, oxygenated with 95% O2-5% CO2). From a hemisected brain, the septum and hippocampus along with the interconnecting fibers were carefully and rapidly dissected out using a microspatula. The preparation was trimmed in ice-cold high-sucrose solution (same contents as the high-sucrose solution listed above) using fine scissors to remove any remaining cortical tissue and the septum. Then, the surface of the preparation was cut at a ~45° angle to expose the pyramidal layer of CA1. The cut enabled visually guided patch-clamp recordings of pyramidal cells which yielded a higher success rate for whole-cell recordings compared to the blind-patch technique used previously. The visual approach allowed identification of CA1 pyramidal cells by their soma location, morphology and the lack of PV-tdTomato fluorescence in the soma. The hippocampal preparation was then left to equilibrate in oxygenated room-temperature high-sucrose solution for 30 min – 1 h before recording. The preparation from only one hemisphere was used for recording from each mouse, and the preparation from either the left or the right hemisphere was chosen randomly for each experiment. Three mice were used in total; we used three intact hippocampal preparations from these mice (one from each mouse) and one pyramidal cell was recorded from each preparation, except for one preparation from which two cells were recorded.
All electrophysiological recordings were performed at 30 ± 2°C, using artificial cerebrospinal fluid (aCSF) containing (in mM) 126 NaCl, 24 NaHCO₃, 10 glucose, 4.5 KCl, 2 MgSO₄, 1.25 NaH₂PO₄, 0.4 ascorbic acid and 2 CaCl₂ (pH 7.3, oxygenated with 95% O₂, 5% CO₂). The hippocampal preparation was placed in a custom-made submerged recording chamber lined with a nylon mesh, and firmly stabilized by carefully placing several lead weights at both septal and temporal poles of the hippocampal preparation. We placed the hippocampal preparation in the recording chamber, such that the CA1 was the most superficial and accessible sub-region for visualization and whole-cell recordings. Recordings were restricted to neurons located within the middle portion of the hippocampus (intermediate between septal and temporal poles of the preparation). The preparation’s stability in the recording chamber was extremely important as aCSF was perfused at the rate of 20–25 ml/min during recordings. Since the tissue is several millimeters thick, such a fast perfusion rate is necessary to ensure sufficient oxygenation. This fast perfusion rate is also required to generate intrinsic theta oscillations from intact hippocampal preparations. In order to achieve temperature stability, aCSF was pre-heated using an electric skillet and further regulated via an automatic temperature controller (Warner Instruments, Hamden, CT). The electrophysiology setup was equipped with an upright BX51W1 Olympus microscope, a 20× water-immersion objective, Nomarsky optics, an infrared camera (Cohu, San Diego, CA), a variable-wavelength fluorescence system (PTI, Mornmouth Junction, NJ) and a monochrome digital camera for fluorescence imaging (DAGE-MTI, Michigan City, IN). Patch pipettes were pulled from borosilicate glass capillaries (2.5–4 MΩ) and filled with the intra-pipette solution containing (in mM) 144 K-gluconate, 10 HEPES, 3 MgCl₂, 2 Na₂ATP, 0.3 GTP, 0.2 EGTA, adjusted to pH 7.2 with KOH. The patch electrode was controlled using a motorized micromanipulator (Sutter Instruments, Novato, CA). An Axopatch-1C amplifier (Axon Instruments, Foster City, CA) and pClamp9 software (Molecular Devices, Sunnyvale, CA) were used for recording. The junction potential was estimated at -15.2 mV and was corrected for. All drugs were obtained from Sigma-Aldrich (St. Louis, MO), unless otherwise noted.

**Intrinsic property characterization.** Intrinsic properties were characterized in current-clamp mode following published protocols with minor modifications. A mixture of synaptic blockers was used to inhibit synaptic activity: 5 μM 6,7-dinitroquinoxaline-2,3-dione disodium salt (DNQX), 5 μM bicuculline and 25 μM DL-2-amino-5-phosphonopentanoic acid sodium salt (DL-AP5) (Abcam, Toronto, Canada). Data analysis was done using custom Matlab software (MathWorks, Natick, MA). Once the whole-cell configuration was achieved, the cell’s resting membrane potential was noted and its spontaneous firing, if any, was recorded for 30 s. Access resistance and resting membrane potential were checked at regular intervals (every ~5 min) throughout the recording of the cell.

The frequency-current (f-I) profiles of the pyramidal cells are important to characterize, as we aim for our single cell model to respond to a variety of synaptic input strengths with frequencies similar to that observed experimentally. These f-I curves were determined by applying depolarizing current steps of 1 s duration to cells held in current clamp. Amplitudes were increased incrementally with step sizes of 25 pA for one of four cells, and 10 pA for three of four cells. The initial firing frequency was determined based on the inverse of the first inter-spike interval, and the final frequency was based on the inverse of the last inter-spike interval in the 1-second depolarizing step. For each cell, the approximate linear slope of the f-I curve above 5 Hz was determined using a least squares method. These values were chosen since above 5 Hz the slope was well-approximated by linearization. In addition, the minimum amount of current required to initiate a spike, the rheobase current (I_rheo in pA), was determined. The action potential threshold was set to be the first voltage point such that the slope of the membrane potential exceeded 20 mV/ms. The spike width was determined at the threshold value. In addition, the spike height from threshold and the minimum membrane potential reached following the spike were measured. Recordings were kept for analysis only if the neuron remained stationary: spikes overshoot 0 mV (-15 mV junction potential corrected) and access resistance < 30 MΩ. While the cell was held at -52 mV in current clamp, as series of 1 s hyperpolarizing steps (25 pA increments) were used to record the post-hyperpolarization rebound spiking. For the figure showing this rebound spiking (Figure 1), the spike artifact in the current clamp input trace (shown in grey) was removed and replaced with the mean current for visualization purposes.

**Mathematical model**

We built a pyramidal cell model based on Izhikevich’s simple spiking model structure. We chose this model as it captures the cell’s ability to produce rebound spiking, the approximate spike shape, and the frequency-current profile of the cell, including spike-adaptation. Thus, this model is relatively simple, but allows one to capture important biophysical properties of pyramidal cells.

The model has a fast variable representing the membrane potential, \(V\) (mV), and a slow “recovery” current given by the variable \(u\) (pA). In order to capture the spike width at threshold, we slightly modified the Izhikevich model by using a different “\(k\)” parameter above and below the spike threshold (\(k_{\text{high}}\) and \(k_{\text{low}}\) respectively). The model is given by:

\[
\begin{align*}
C_m \frac{dV}{dt} &= k(V-v_r) (V-v_l) - u + I_{\text{applied}} + I_{\text{shift}} \\
u &= a [b (V - v_r) - u] \\
\text{if} \quad V \geq v_{\text{peak}} \quad \text{then} \quad u &\leftarrow c, u \leftarrow u + d \\
\text{Where} \quad k &= k_{\text{high}} \quad \text{if} \quad V \leq v_r; \quad k &= k_{\text{low}} \quad \text{if} \quad V > v_r
\end{align*}
\]

The parameters are as follows:

- \(C_m\) (pF) is the membrane capacitance.
- \(v_r\) (mV) is the resting membrane potential.
- \(v_l\) (mV) is the instantaneous threshold potential.
- \(v_{\text{peak}}\) (mV) is the spike cut-off value.
- \(I_{\text{applied}}\) (pA) is the applied current, and represents the applied input into the cell.
- \(I_{\text{shift}}\) is a current that shifts the f-I curve laterally to allow the model to easily capture the rheobase current.
$a$ (ms$^{-1}$) is the recovery time constant of the adaptation current.

$b$ (nS) describes the sensitivity of the adaptation current to sub-threshold fluctuations. Greater values couple $V$ and $u$ more strongly resulting in possible subthreshold oscillations and low-threshold spiking dynamics. Further, the sign of $b$ determines whether the effect of $u$ is amplifying ($b < 0$) or resonant ($b > 0$).

$c$ (mV) is the voltage reset value.

$d$ (pA) is the total amount of outward minus inward currents activated during the spike and affecting the after-spike behaviour.

$k$ (nS/mV) represents a scaling factor. $k_{\text{high}}$ is used to adjust the spike width after the threshold.

As with the experimental frequency-current (f-I) curve frequencies, we exhibited the “initial” and “final” f-I curves for each model, where the initial curves were based on the inverse of the first interspike interval (ISI) due to a one second current step, and the final curves were based on the inverse of the last ISI. A linear fit based on the least squares method (on frequencies over 10 Hz) was done for each curve (using 5 Hz gave essentially the same results). We then chose parameters in which our models exhibited similar initial and final f-I curves to those of the experimental pyramidal cells. To do so, we first set the resting membrane potential at the rheobase, the spike threshold, the minimum potential reached by the spike after-hyperpolarization, the spike peak, and the spike width at threshold (providing us with values for $v_r, v_t, c, v_{\text{peak}},$ and $k_{\text{high}}$ respectively) based on our experimentally determined values (see Results). The threshold is defined in “Intrinsic Property Characterization”. Since our pyramidal cells exhibited resonant properties, we considered $b$ values such that $b > 0$. We initially held $b$ and $k_{\text{low}}$ constant (at 0.2 nS and 0.05 nS/mV), and varied $a$ between 0 and 1 with an initial step size of 0.01, and $d$ between 0 and 20 with a step size of 1. Choosing our $a$ and $d$ parameters that returned the best fits to our initial and final slopes, we then varied $b$ between 0.1 and 10, and $k_{\text{low}}$ between 0 and 20 (both with a step size of 0.1). Noting that we required more adaptation, we then returned to vary $a$ between 0 and 0.1 with an initial step size of 0.0001, and $d$ again between 0 and 20 with a step size of 1. The model was simulated using Brian software$^{15}$.

Results
Using the described whole hippocampal preparation and recordings from four CA1 pyramidal cells (from three mice), we developed our simple biologically-based cellular models. Our goal is to obtain representative CA1 pyramidal cell models that capture the essence of the experimental data in the described experimental context. By biologically-based, we mean that passive properties and spike characteristics are captured. Specifically, resting potential, spike threshold, spike width, spike peak and after-hyperpolarization potentials were incorporated into our models. In addition, the adaptation characteristics determined from the frequency-current (f-I) curves

Figure 1. An example of rebound firing in a CA1 pyramidal cell. While the cell was held at -52 mV in current clamp, two 1-s hyperpolarizing steps (shown in grey; top: 25 pA, bottom: 50 pA) were used to record the post-hyperpolarization rebound spiking (voltage traces shown in black). For visualization purposes, the spike artifact in the current clamp input trace was removed and replaced with the mean current.
(see Methods) are captured. Rebound firing (from inhibition or hyperpolarization) has been shown in several experimental studies\(^6,17\) and is an important consideration in population theta activities. As shown in Figure 1, we could obtain rebound firing in our CA1 pyramidal cells, thus justifying their inclusion in our models.

Analysis of the experimental data yielded the following: at rheobase, the pyramidal cell membrane potential rested at -61.8 ± 2.9 mV (mean ± SEM), the spike threshold was -57.0 ± 2.2 mV, the after hyperpolarizing potential reached a minimum of -65.8 ± 3.83 mV, and the spike reached a peak at 22.6 ± 19.9 mV (n=4 cells). The spike width at threshold, was 3.6 ± 0.48 ms. Thus, we set \(v_r = -61.8\) mV, \(v_t = -57.0\) mV, \(c = -65.8\) mV, \(v_{peak} = 22.6\) mV, and \(k_{high} = 3.3\) nS/mV in our models (see Methods). The remaining model parameters were chosen such that the rheobase and f-I curves of the cell model were similar to those of the cell recordings. To do so, we first considered the f-I curves of the cell recordings (Figure 2). To demonstrate the amount of adaptation that the cell exhibited, we created two f-I curves for each cell: one based on the first inter-spike interval (ISI) of the cell’s spiking during a one second current step (denoted initial curve, data points shown as asterisks in Figure 2), and one based on the last (final curve, data points shown as squares in Figure 2). If the cell only had one spike in the 1s trace, a frequency of 1 Hz was given. We note that two of our recordings (Pyramidal cell 1 and Pyramidal cell 2, shown in red and blue in Figure 2) exhibited stronger adaptation than the other two (Pyramidal cell 3 and 4, shown in green and black in Figure 2). Thus, we created pyramidal cell models based on the strongly adapting cells and the weakly adapting cells separately. While adaptation clearly exists (e.g., here 18,19), biological variability, precise protocols and contexts need to be considered. As such, we did not aim to exactly capture adaptation characteristics, but rather to capture strongly and weakly adapting cells as represented by the data here. Also, since our model has a simple, mathematical structure, it is limited in the extent of biologically-based characteristics that it can encompass.

**Strongly adapting model**

It is important that our model f-I curve captures two important properties of the experimental data: the rheobase current (i.e. the minimum amount of current required to initiate a spike), and the approximate slope of the curve. If these properties are captured, then the model will spike with similar frequencies as the physiological cell given the same level of synaptic input, at least to a first approximation. We found that for the two strongly adapting pyramidal cells (1 and 2), the slope of the linear least squares approximation of the f-I curves above 5 Hz were 0.376 and 0.385 for the initial curves, and 0.030 and 0.040 for the final curves. Again, the initial frequencies are based on the inverse of the first inter-spike interval due to a one second current step, and the final frequencies are based

![Figure 2. The initial and final frequency current profiles for the four pyramidal cell recordings (from three mice) in the CA1 region of the intact hippocampal preparation in vitro.](image-url)
on the last inter-spike interval. A series of depolarizing (25 and 10 pA) steps were used to determine the rheobase currents, which were 1.2 pA and 38.7 pA for the two strongly adapting cells (f-I curves, red and blue curves in Figure 2 or data in Figure 3).

We kept our previously determined parameters constant (i.e. \( v_r = -61.8 \text{ mV} \), \( v_t = -57.0 \text{ mV} \), \( c = -65.8 \text{ mV} \), \( v_{\text{peak}} = 22.6 \text{ mV} \), and \( k_{\text{high}} = 3.3 \text{ nS/mV} \)), and set our membrane capacitance to \( C_m = 115 \text{ pA} \). We then varied the parameters \( a, b, d, \) and \( k_{\text{low}} \) to produce multiple models. We determined the rheobase current and the slope of the initial and final f-I curve over 10 Hz (using a least squares approach) for each model in order to settle upon a final model in which our initial and final f-I slopes and rheobase approximated that which we determined biologically. We determined that \( a = 0.0012 \text{ ms}^{-1} \), \( b = 3 \text{ nS} \), \( k_{\text{low}} = 0.1 \text{ nS/mV} \), \( d = 10 \text{ pA} \), and \( I_{\text{shift}} = 0 \text{ pA} \). This gave us a model f-I initial slope of 0.432, a final slope of 0.099, and a rheobase of ~0 pA (see Figure 2). As shown in Figure 4, the model shows strongly adapting firing (Figure 4A) and rebound firing when hyperpolarized (Figure 4B).

Weakly adapting models
Following a similar methodology, we created two separate models for the weakly adapting pyramidal cells: the first better captures the cell’s weak adaptation, especially for larger currents, but has a steep final slope, whereas the second captures the more gradual slope of the final f-I curve, but doesn’t exhibit the cell’s weak level of adaptation.

We found that for the two weakly adapting pyramidal cells, the slope of the linear least squares approximation of the f-I curves were 0.119 and 0.138 for the initial curves, and 0.013 and 0.044 for the final curves (values relating to experimental, data green and black in Figure 2 and Figure 5). A series of depolarizing (10 pA) steps were used to precisely determine the rheobase currents, which were 62.0 pA and -12.1 pA for the two weakly adapting cells. We kept our previously determined parameters constant (i.e. \( v_r = -61.8 \text{ mV} \), \( v_t = -57.0 \text{ mV} \), \( c = -65.8 \text{ mV} \), \( v_{\text{peak}} = 22.6 \text{ mV} \), and \( k_{\text{high}} = 3.3 \text{ nS/mV} \)), and set our membrane capacitance to \( C_m = 300 \text{ pA} \), which allowed us to obtain the gradual f-I slope. We then varied the parameters \( a, b, d, \) and \( k_{\text{low}} \) to produce multiple models, and again determined the rheobase current and the slope of the initial and final f-I curve over 10 Hz (using a least squares approach) for each model. For our first model, we determined that \( a = 0.001 \text{ ms}^{-1} \), \( b = 3 \text{ nS} \), \( k_{\text{low}} = 0.5 \text{ nS/mV} \), \( d = 5 \text{ pA} \), and \( I_{\text{shift}} = -45 \text{ pA} \). This gave us a model f-I initial slope of 0.136, a final slope of 0.089, and a rheobase of 5 pA (see purple solid and dashed lines in Figure 5). The second weakly adapting model is identical to the first, except that we explored smaller \( a \) parameter values in order to capture the gradual slope of the final

![Figure 3](image-url)  
**Figure 3.** The strongly adapting pyramidal cell f-I curves (Pyramidal cells 1 and 2 shown in blue and red respectively) are shown against the strongly adapting pyramidal cell model (dark green). The initial data points are shown as asterisks and the final points shown as squares. The initial model curve is shown as a solid line (initial slope: 0.432), and the final curve shown as a dashed line (final slope: 0.099). The model rheobase (~0 pA) and slope approximate those determined experimentally.
Figure 4. **A**: An example intracellular recording of Pyramidal cell 1 during current clamp with applied current of 188 pA (top, blue) is compared with the firing of our strongly adapting pyramidal cell model, also with an applied current of 188 pA (bottom, dark green). The firing rates and amount of adaptation of the model are similar to those of the experiment. **B**: Two examples of rebound firing in our strongly adapting model. In each case, a one-second step of hyperpolarizing input is applied (shown as dashed lines; top: 20 pA step, bottom: 50 pA step). In each case, the strongly adapting model produces rebound spiking (solid line), where more spiking occurs for larger amounts of hyperpolarizing input.
The initial data points are shown as asterisks and the final points shown as squares. The initial model curve is shown as a solid line (initial slope: 0.136), and the final curves are shown as dashed lines. Model 1 exhibits less adaptation (final slope for model 1: 0.089; final slope for model 2: 0.048), but higher final frequencies than model 2 (compare purple and magenta dashed lines). The model rheobase (5 pA) and slopes approximate those determined experimentally.

Discussion and conclusion
We have developed simple, biologically-based cellular models of pyramidal cells from CA1 hippocampus. These models capture the frequency-current profiles of both strongly and weakly adapting cells. Importantly, we have used pyramidal cell recordings from a well-defined experimental context as a basis for our model development. We note that even though other simple pyramidal cell models exist with a conductance-based biophysical representation, it is challenging to have clear links with adaptation or rebound firing characteristics as exists in pyramidal cells (e.g., see 21). We note that while modifications have been done to such simple models (e.g., Stark et al.15 used the Olfusen et al. model11 which incorporated sodium currents, potassium current, voltage-dependent M currents, and a leak current, and added an h-current based on 24 to incorporate rebound capabilities), the resulting cellular model outputs constraints with respect to experimental data are unclear, and as such, we consider them not to be biologically-based per se.

Our models do not include the multiple voltage-gated channels known to be present in pyramidal cells, and are not spatially extended by being multi-compartment in nature. Multi-compartment, biophysical models of CA1 pyramidal cells exist as well as single-compartment biophysical models with various voltage-gated channels, but the goals in developing those models are different. Here, we are interested in capturing cellular characteristics in a well-defined experimental context (for subsequent large network explorations that take advantage of the experimental context), whereas these other studies have considered, for example, conductance balances to understand how they contribute to cellular output. We further note that the richness of detail in CA1 pyramidal cells is expanding (e.g., see 19 in which countermodulation by metabotropic receptors in bursting or regular spiking pyramidal cells was shown). In essence, it is always the case that the mathematical models are a limited representation of the biology.
In previous work, we used adaptation characteristics from the literature to develop simple models of CA3 pyramidal cell models, and showed that population bursting could occur in excitatory networks if the adaptation characteristics were in line with the experimental data. In this work we had a full set of experimental recordings and so could capture appropriate cellular characteristics more directly. Although there should not be large differences in some cellular characteristics (e.g., spike widths etc.), there could be differences in characteristics such as rheobase and adaptation amounts due to varying experimental contexts (e.g., solutions, recording setup details and so on — see 16–19). Coupled with biological variability, it would be additionally challenging to be clear about model limitations in subsequent model usage. Here, with our simple mathematical model representation and knowledge of the biological variability in hand, one is easily aware of any changes in the parameters of the model that would result in large deviations from the experimental data. In doing this work, we have been clear about the rationale and manner in which the parameter choices were made. Generalization of the parameter choices are possible and could be considered, but should be done such that modeling and experimental details and contexts are not completely separated.

We note that robust fitting strategies of experimental data to simple, mathematical representations of neurons are being developed. However, there are some differences in the modeling goals. In the paper by Hertäg et al., the goal was to use the developed models based on in vitro recordings to predict spiking in an in vivo context. Here, we have developed our cellular models in the experimental context for which we are building network models to help determine mechanisms occurring in the biological system. One can consider

Figure 6. A: An example intracellular recording of Pyramidal cell 3 during current clamp with applied current of 154 pA (top, light green) is compared with the firing of our weakly adapting pyramidal cell models, also with an applied current of 154 pA (model 1: middle, purple; model 2: bottom, magenta). The firing rates and amount of adaptation of the model are similar to those of the experiment. B: An example of rebound firing in our weakly adapting model 1. A one-second step of 1000 pA hyperpolarizing input is applied (dashed line). The weakly adapting model produces rebound spiking (solid line), but requires a reasonably large amount of applied input. The weakly adapting model 2 does not produce rebound spiking following steps of hyperpolarizing input in the physiological range.
using our models in other contexts, keeping in mind the limitations associated with the models as developed. In essence, when incorporating various cellular characteristics, one should express the choices, rationale and reasoning behind the model development, which naturally stem from the modeling goals.

In conclusion, with our simple, developed models as presented here, we can proceed to considering very large networks that include these models in this experimental context. Furthermore, our simple model representations will also allow us to take advantage of developed theoretical analyses\(^{26,30}\).

**Data availability**

ZENODO: Data set of CA1 pyramidal cell recordings using an intact whole hippocampus preparation, including recordings of rebound firing (V2), DOI: 10.5281/zenodo.17794\(^1\).

ModelDB: CA1 pyramidal neuron, available at http://senselab.med.yale.edu/ModelDB/ShowModel.cshtml?model=182515.

**Author contributions**

KAF and FKS conceived the study. CYLH, BA, SW designed the experiments. CYLH, BA carried out the experiments. KAF carried out the modeling and data analysis. FKS and KAF prepared the first draft of the manuscript. All authors were involved in the revision of the draft manuscript and have agreed to the final content.

**Competing interests**

No competing interests were disclosed.

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Alia Borisyuk
Department of Mathematics, University of Utah, Salt Lake City, UT, USA

The article presents minimal models for CA1 pyramidal cells, based on fitting the frequency-current curves that had been experimentally recorded in whole hippocampus preparation. There are two types of models, differing in some parameter values, to account for “strongly” and “weakly” adapting cell varieties. The goal of the present work is to present the models and their basic fit to single cell data, in preparation for future large network studies.

Comments:
I think this work would be much stronger if testable predictions were generated from the models. For example, what would be the responses to time varying inputs and how the responses would differ between the strongly and weakly adapting cells?

It is not clear to me that obtaining one model for each variety of cells is sufficient. For example, two strongly adapting cells have very different rheobase current values. If you fit the model to each cell individually, I expect that you will end up with two very different parameter sets. What would be the consequences for responses to time varying inputs, for example? Considerations like these will be very important when you decide how much variability and in which parameters to include in the network model. This is also related to the fact that a single model was not able to capture all desired properties of the weakly adapting model. I would like to see more discussion on the consequences of the spectrum of models for future network work.

Competing Interests: No competing interests were disclosed.

I confirm that I have read this submission and believe that I have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Frances Skinner, University Health Network, Toronto, Ontario, Canada
We would like to thank the reviewer for their helpful comments, which we will be taking into consideration.

We would like to point out that we focused on the single cell model and did not try to also include network simulations in this article as it was originally submitted as a 'Short Research Article' type.

However, F1000Research recently replaced the 'Short Research Article' category with a shorter 'Research Notes' article type. As this article did not fit the criteria of a 'Research Note', it appears as a 'Research Article' instead.

**Competing Interests:** No competing interests were disclosed.

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**Author Response 19 May 2015**

**Frances Skinner**, University Health Network, Toronto, Ontario, Canada

We agree that it is may not sufficient to have one model for each of the variety of cells, and that it would be good to consider consequences of time varying input. However, as mentioned in our more immediate response, this work was to present the cellular model together with the experimental data. We were not aiming for testable predictions from the cellular models on their own, but we are aiming to use them in network models to help determine mechanisms in the biological system (see added abstract references), by focusing our models on the experimental context so that there can be a back and forth examination between model and experiment, given that the model will always be limited and the experimental details can vary between different contexts. Since we have a clear sense of the rationale and limitations of the cellular model, model network mechanistic insights would be viewed through those lenses and help determine what modeling and experimental work should be further examined.

For the time varying input aspect, this was raised (in a different way) by the other reviewers (see their point 6), and we have revised the paper accordingly. In essence, we see the fits as trying to match the experimental data to a first approximation.

For the issue of different weakly and strongly adapting characteristics, please see our response to the other reviewers (point 4).

**Competing Interests:** No competing interests were disclosed.

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**Reviewer Report 05 June 2014**

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**Farzan Nadim**  
Department of Biological Sciences, New Jersey Institute of Technology, Newark, NJ, USA
A simple mathematical yet biological model of hippocampal CA1 pyramidal cell has been developed to capture the cellular characteristics (f-I curve, rheobase current, firing rate adaptation and rebound spiking) of those neurons in an intact preparation of hippocampus.

Although this study does not examine any biological question or hypothesis directly, the simplified models of CA1 pyramidal cells, in conjunction with a similar model of the fast spiking interneurons previously developed by this lab, can be used in future modeling studies that explore the network properties in the hippocampus.

Comments:

1. First paragraph of the Introduction:

   "To address this recognized difficulty we are developing models that are based on well-defined experimental contexts in which both the cellular and the network aspects of the models can be considered simultaneously."

   Please specify more clearly about the network aspects, you are referring to.

2. First paragraph of Introduction:

   "Using such models, we aim to help determine, predict and test biologically based mechanisms."

   This is a bit misleading. In this work, the model only replicates biological behavior of neurons. There is no clear prediction of any biological phenomenon.

3. End of the second paragraph of Introduction:

   "we can build and examine several large network models that are aligned with the biology. Subsequent analyses of these large network models could determine the mechanisms by which particular cellular characteristics critically contribute to the population activities observed in our experimental context."

   It would be more exciting to construct network models and make biological predictions. Construction of simple cellular models to capture biological characteristics of individual neurons is not novel. In fact, the authors have used similar modeling approach to develop models in references 6 and 23.

4. Second paragraph of Results - Stronger adaptation vs weaker adaptation - Has it been shown before? If yes, please include some references here. If not, I am wondering if it would be worthwhile to check the adaptation by comparing steady-state ISIs. Maybe different neurons have different time course of adaptation but at the end they show same level of adaptation.

5. If we run the model for longer duration, how does the behavior change, does it continue to adapt or it reaches a steady-state?
6. Second paragraph of Strongly adapting model:

"If these properties (f-I curve, rheobase current and adaptation) are captured, then the model will spike with similar frequencies as the physiological cell given the same amount of synaptic input."

Is the applied protocol (continuous injections of currents for 1s) sufficient to characterize the response of these neurons in the presence of synaptic inputs?

7. Second paragraph of Weakly adapting models:

"In addition, to obtain an appropriate rheobase current, we included a short in the applied current."

I do not understand why $l_{shift}$ term is included in $l_{applied}$ to adjust rheobase?

8. Third paragraph of Discussion and conclusion:

"In previous work, we used adaptation characteristics from the literature to develop simple models of CA3 pyramidal cell models, and showed that population characteristics were in line with the experimental data."

It would be interesting and more insightful to see how this work can be extended to network models as has been done previously (in references 6 and 23) by the authors.

9. Third paragraph of Discussion and conclusion:

"Here, with our simple mathematical model representation and knowledge of the biological variability in hand, one is easily aware of any changes in the parameters of the model that would result in large deviations from the experimental data."

This is very important aspect. But that would only be possible if the effects of parameters can be characterized. It would be interesting to see any such generalizations.

10. Fourth paragraph of Discussion and conclusion:

"Here, we have developed out cellular models in the experimental context for which we build the network models to determine physiologically-based mechanisms."

Building network models incorporating CA1 pyramidal cells and determining physiologically-based mechanisms is clearly not presented in this paper and should be indicated as future work.

11. In Figure 3, please also show rebound firing of recorded cells, if available.

12. In Figure 2, the label pointing to green dotted line is misspelled. It should be final curve instead of "finial curve".

**Competing Interests:** No competing interests were disclosed.
We confirm that we have read this submission and believe that we have an appropriate level of expertise to confirm that it is of an acceptable scientific standard.

Author Response 24 Jun 2014
Frances Skinner, University Health Network, Toronto, Ontario, Canada

We would like to thank the reviewers for their helpful comments. We will respond more specifically and revise our article accordingly in the near future.

We would like to point out that we focused on the single cell model and did not try to also include network simulations in this article as it was originally submitted as a 'Short Research Article' type. However, F1000Research recently replaced the 'Short Research Article' category with a shorter 'Research Notes' article type. As this article did not fit the criteria of a 'Research Note', it appears as a 'Research Article' instead.

Competing Interests: No competing interests were disclosed.

Author Response 19 May 2015
Frances Skinner, University Health Network, Toronto, Ontario, Canada

1-2: We have revised manuscript to make these points clear.

3: We agree. As mentioned in our more immediate response, this ‘short report’ was to present the cellular model. Network simulations using these models have been done (presented at CNS and SfN meetings), and the manuscripts are in preparation. These abstract references have been added.

4: Although it is clear that spike frequency adaptation can occur in CA1 pyramidal cells (as in additional figure and references), to the best of our knowledge, a specific distinction between strongly and weakly adapting has not been described in the literature for CA1 pyramidal cells, although such distinctions have been reported for CA3 pyramidal cells (Hemond et al., 2008). This is a challenging issue to be clear and distinct about due to both experimental and modeling limitations since the biophysical basis of spike frequency adaptation itself is not completely clear. For example, “… In most studies, however, the initial, steady-state, or mean firing frequency were not controlled…” (from Discussion in Fernandez and White, 2010). They were referring to $I_M$ current, but this points to the potential importance of details in different experimental contexts when comparing particular features. So, examination of the biophysical basis underlying adaptation have been explored (e.g., see Discussion in Fernandez and White 2010 ref as cited from above), and also, Ascoli et al. (2010) has shown that rebound is rarely observed in physiological conditions, and it can be unmasked by blocking A-type currents.

Our intention here is not to say that there are two distinct types of adapting CA1 pyramidal models per se. For our models here, we aimed to be clear about how they were ‘biologically-based’ using our given context based on f-I curves, resting potential etc., but do not have a biophysical basis in terms of voltage-gated channels etc. Strongly and weakly adapting characteristics were observed (and modeled), but we think that it would be premature to suggest that this is a distinct (biological) separation without trying to dissect out the biophysical basis, doing more recordings of longer
durations and so on. For our work here, the goal was to develop models based on a clear experimental context.

We agree that this whole aspect needs to be explored fully and in more detail in future work, but we also think that it is important that this be done without separation of experiment and model details and context, and goals.

5: The model has reached a steady-state by the end of the first second, and thus this steady-state is reflected in our model final f-I curve.

6: We agree that the applied protocol used is not sufficient to characterize response to synaptic input. We have revised the particular sentence so that it is clear that we simply mean ‘to a first approximation’ (and would only mean ‘tonic’ input of the level of synaptic input).

7: Due to the simplicity of the model, it was difficult to capture the rheobase as well as the initial and final frequency current profiles in the weakly adapting model, and thus a term was needed to shift the curve laterally (I\text{shift}). However, your comment brought to light that this shift would be more appropriately represented by an independent term directly affecting equation (1), rather than influencing the \text{applied} current. This change in the representation is now reflected in the equation and description.

8: Yes, we agree. See point 3 above.

9: Yes, we agree and have added a couple of sentences to the Discussion in this regard.

10: We have revised that sentence accordingly and refer to abstracts of ongoing work.

11: Experimental data showing rebound firing is now included.

12: Fixed.

**Competing Interests:** No competing interests were disclosed.
