Charm- and Bottom-Quark Production in Au+Au Collisions at $\sqrt{s_{NN}} = 200$ GeV

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The invariant yield of electrons from open-heavy-flavor decays for $1 < p_T < 8$ GeV/c at midrapidity $|y| < 0.35$ in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV has been measured by the PHENIX experiment at the Relativistic Heavy Ion Collider. A displaced-vertex analysis with the PHENIX silicon-vertex detector enables extraction of the fraction of charm and bottom hadron decays and unfolding of the invariant yield of parent charm and bottom hadrons. The nuclear-modification factors $R_{AA}$ for electrons from charm and bottom hadron decays and heavy-flavor hadrons show both a centrality and a quark-mass dependence, indicating suppression in the quark-gluon plasma produced in these collisions that is medium sized and quark-mass dependent.

I. INTRODUCTION

Charm ($c$) and bottom ($b$) quarks, with masses of $m_c \approx 1.3$ GeV/$c^2$ and $m_b \approx 4.2$ GeV/$c^2$, are much heavier than the temperature reached in the quark-gluon plasma (QGP) produced at the Relativistic Heavy Ion Collider (RHIC) and the Large Hadron Collider (LHC). As such, charm and bottom quarks, collectively known as heavy-flavor quarks, are produced predominantly at the primordial stages of high-energy nucleus-nucleus collisions and negligibly via interactions between thermalized particles in the QGP. Once produced, heavy quarks lose energy while propagating through the QGP and, for that reason, open-heavy-flavor hadrons are excellent probes of the properties of the QGP. The current status of both experimental and theoretical developments is reviewed in Ref. [1].

Experiments at RHIC and the LHC have measured the cross section of inclusive heavy flavor, as well as those for charm and bottom separated final states [2–11]. Previous measurements of separated charm and bottom-heavy-flavor cross sections at RHIC, obtained in minimum-bias (MB) Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV by the PHENIX Collaboration, suggest lower suppression of electrons from bottom hadron decays $b \rightarrow e$ compared to those from charm-hadron decays ($c \rightarrow e$) in the range of $3 < p_T < 4$ GeV/c [12]. This is in agreement with the widely postulated mass ordering for energy loss by quarks ($q$) and gluons ($g$) in the QGP, $\Delta E_q > \Delta E_{u,d,s} > \Delta E_c > \Delta E_b$ at $p_T > 4$ GeV/c. Due to the large systematic uncertainties on the $p+p$ baseline measurement, the nuclear-modification factor $R_{AA}$ did not definitively constrain the suppression pattern and mass dependence of the energy-loss mechanism.

Although heavy-flavor hadron-production mechanisms have been studied widely, the mechanisms that contribute to the in-medium hadronization thereof are not well understood. Many classes of models exist that employ one or more of the following effects: radiative energy loss [13, 14], collisional energy loss [15], or dissociation and coalescence [16] of heavy-flavor hadrons in the medium. While radiative energy loss is significant at high $p_T (> \approx 10$ GeV/c), theoretical models suggest that collisional energy loss is equally important at low $p_T$ [10]. Cold-nuclear-matter effects, such as the Cronin effect for heavy quarks, could also play an important role in the interpretation of these observations at low to medium $p_T$ [17]. For these reasons, a precise measurement of the nuclear-modification factor $R_{AA}$ over a broad range of momentum and centrality is necessary to investigate the interplay between competing mechanisms that could contribute to the suppression or enhancement seen in different regions of phase space.

This paper reports on the measurement of electrons from semileptonic decays of open charm and bottom hadrons at midrapidity $|y| < 0.35$ in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. Using the combination of the high-statistics data set recorded in 2014 and the updated $p+p$ reference from 2015 [18], nuclear-modification factors $R_{AA}$ of separated charm and bottom electrons in MB Au+Au as well as four centrality classes in Au+Au can be measured with improved precision compared to our previously published results [12].

This paper is organized as follows: Section II provides a brief introduction to the PHENIX detector, with special emphasis on the central arm detectors pertinent to this measurement. Section III details track reconstruction, electron identification, event selection, background estimation, signal extraction, and unfolding. Section IV describes systematic-uncertainty estimates. Section V provides the results of the measurement, along with comparisons with theoretical models. Finally, Section VI gives
the summary and conclusions.

II. EXPERIMENTAL SETUP

PHENIX has previously published the decay-electron contribution from charm and bottom decays separately [12, 18] through the combination of electron-identification detectors in the central arms covering $|y| < 0.35$, and the measurement of event-vertex and decay-electron trajectories provided by an inner silicon tracker (VTX). The detector systems relevant to this measurement are discussed below, while a detailed description of the PHENIX detector is given in Refs. [19–21].

The VTX is described in detail in Refs. [13, 22]. It is composed of two arms, each with $|\eta| < 1$ and $\Delta \phi \approx 0.8 \pi$ coverage. Each arm has four layers around the beam pipe. The radial distances of these layers from the nominal beam center are 2.6, 5.1, 11.8, and 16.7 cm. The innermost two layers have pixel segmentation of $50 \times 425 \ \mu m$. The two outer layers have strip segmentation of $80 \times 1000 \ \mu m$.

III. ANALYSIS METHOD

This paper reports measurements using data collected by the PHENIX experiment during the 2014 high-luminosity Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV. The data were recorded with a MB trigger and correspond to an integrated luminosity of 2.3 nb$^{-1}$. A set of event, offline track and electron selection cuts were applied as described below.

A. Event selection

Events considered here are characterized by the MB trigger, which requires simultaneous activity in both beam-beam-counter (BBC) phototube arrays located at pseudorapidity $3.0 < |\eta| < 3.9$ and the zero-degree calorimeter at 18 m downstream from the intersection point. This criterion selects $93 \pm 2\%$ of the Au+Au inelastic cross section. The total number of charged particles as measured by the BBC determines the collision centrality. The BBC is also used later to calculate the number of nucleon participants and the number of binary collisions via comparisons with Monte-Carlo-Glauber model simulations of the collisions [23]. The results shown here are for MB Au+Au collisions and 0%–10%, 10%–20%, 20%–40% and 40%–60% centrality classes.

The collision vertex is determined by clusters of converging VTX tracks. The vertex resolution is determined from the standard deviation of the difference between the vertex position measured by each VTX at the east and west arm. The vertex resolutions for $x-y-z$ coordinate are $(\sigma_x, \sigma_y, \sigma_z) = (44, 38, 48) \ \mu m$. The radial beam profile during the 2014 run had a width of 45 $\mu m$ and was very stable during beam fills. The beam-center position in the $xy$ plane was then determined from the average position during the fill to avoid autocorrelations between the vertex determination and the distance of closest approach (DCA) measurements in each event. Because of the modest RHIC collision rates in 2014 of less than 10 kHz in Au+Au collisions, no significant contributions were found of multiple collisions per beam crossing or signal pileup in the dataset. The analysis required a z-vertex within $\pm 10 \ cm$ reconstructed by the VTX detector.

B. Track Reconstruction

Charged-particle tracks are reconstructed (trajectory and momentum) by the PHENIX central-arm drift chambers (DC) and pad chambers covering the pseudorapidity $|\eta| < 0.35$ and azimuthal angle $\Delta \phi = \pi/2$. To identify electrons and positrons, the reconstructed tracks are projected to the ring-imaging Čerenkov Detector (RICH). Electrons and positrons are collectively referred to here as electrons. In the momentum range where charged pions are below the RICH radiator threshold $(p_T < 4.7 \ GeV/c)$, tracks are required to be associated with signals in two phototubes within a radius expected of electron Čerenkov rings. Above this threshold, to aid in eliminating pion background, associated signals in three phototubes are required. Additional tracking information is provided by pad chambers that are immediately behind the RICH.

Energy-momentum matching is also required for electron identification. Electromagnetic calorimeters (EMCal) are the outermost detectors in the PHENIX central arms. The EMCal comprises eight sectors, two of which are lead-glass layers, and six of which are lead-scintillator layers. Tracks with measured momentum $p$ that are associated with showers in the calorimeters of energy $E$ are characterized by the variable $\text{dep} = (E/p - \mu_{E/p}) / \sigma_{E/p}$, where $\mu_{E/p}$ and $\sigma_{E/p}$ are the mean and standard deviation of a precalibrated Gaussian $E/p$ distribution. The requirement of $\text{dep} > -2$ further removes background from hadron tracks associated with Čerenkov rings produced by nearby electrons or high-momentum pions. Remaining background contributions are quantified as discussed below.

The reconstructed tracks are then associated to VTX hits to perform the displaced tracking around the collision vertex. Taking advantage of the different decay lengths of charm and bottom hadrons (viz. for $D^0$ the decay length is $c\tau = 122.9 \ \mu m$ and for the $B^0$ it is $c\tau = 455.4 \ \mu m$ [24]), electrons from these decays are statistically separated based on the DCA$_T$ in the transverse plane (x-y, normal to the beam direction) to the collision vertex. Figure 1 illustrates the definition of DCA$_T = L - R$ for a VTX-associated track, where R is a radius of the circle defined by the track trajectory in
FIG. 1. Definition of the distance of the closest approach DCA\textsubscript{T} in the transverse plane (normal to the beam direction).

the constant magnetic field around the VTX region and L is the length between the beam center and the center of the circle.

C. Background estimation

1. Misreconstruction

In a high-multiplicity environment, tracks are accidentally reconstructed with hits from different particles. Misreconstructed tracks have two sources: (i) misidentified hadrons composed of tracks accidentally matching RICH Čerenkov rings or EMCal clusters; and (ii) mismatches between DC tracks and uncorrelated VTX hits.

The misidentified hadron-track contamination is estimated with a sample of tracks where the sign of their z-direction is swapped. The swapped tracks that, after being projected to RICH, match Čerenkov rings provides the expected number of misidentified hadrons. Charged hadrons with momentum \( p > 4.7 \) GeV/c also radiate Čerenkov light and make RICH hits, meaning the swap method underestimates the fraction of misidentified hadrons. The contamination at high \( p_T \) is estimated by the \textit{dep} template method, in which the measured \textit{dep} distribution is assumed to be the sum of the electron distribution and the hadron-background distribution. The \textit{dep} template for the electron distribution is obtained by the RICH swap method for \( p_T \leq 4.5 \) GeV/c, where the hadron contamination is very small. The \textit{dep} template for hadron backgrounds is obtained by vetoing the electron candidates from all reconstructed tracks. The measured \textit{dep} distribution for \( p_T > 4.5 \) GeV/c is fitted with the electron and hadron background templates. An example of the \textit{dep} template method is shown in Fig. 2 for electron candidates at \( 6 < p_T < 7 \) GeV/c in MB Au+Au collisions. The electron signal in the \textit{dep} distribution is centered at \( \text{dep} = 0 \). The background tail due to hadrons overlaps the signal region. The hadron background increases at higher \( p_T \).

2. Photonic background

Photonic electrons are the main background source in this analysis. They are produced by internal conversions (Dalitz decay) and photon conversions at the beam pipe and the first VTX layer. Photonic conversions produced in the other layers of the VTX do not produce tracks accepted by the tracking algorithm because the presence of a hit in the first layer is required. Electron pairs from converted photons have a small opening angle, therefore it is required that an electron track should not have a neighboring electron track with \( -0.02 < \text{chrg} \times \Delta \phi < 0.04 \) radian for \( p_T < 1.8 \) GeV/c and narrower for high \( p_T \), where chrg is the charge of the track and \( \Delta \phi \) is the azimuthal difference of electron pairs. This isolation cut minimizes the contamination from internal and external conversion electrons, and is the same as described in Ref. [12].

The mismatch between DC tracks and uncorrelated VTX hits is estimated by the VTX swap method, which intentionally creates a mismatch by changing the angle of DC tracks by 10 degrees in the \( \phi-\eta \) plane. The 10-degree rotation is sufficiently larger than the angular resolution of the DC such that the rotated tracks are never connected with VTX hits belonging to the same particle.

The number of electrons obtained after removing background from misidentified and mismatched tracks but before the isolation cut, \( N_e \), is the sum of photonic \( N_P \)
and nonphotonic sources \((N_{NP})\):
\[ N_e = N_P + N_{NP}, \]
while the number of electrons after the isolation cut is
\[ \tilde{N}_e = \varepsilon_P \times \varepsilon_{UC} \times N_P + \varepsilon_{UC} \times N_{NP}, \]
where \(\varepsilon_P\) is the survival rate after the isolation cut for the correlated pairs such as photonic electrons, and \(\varepsilon_{UC}\) is the survival rate for the uncorrelated tracks. The \(\varepsilon_{UC}\) is also applied to both the photonic and nonphotonic electrons because uncorrelated tracks appear everywhere. By solving Eqs. (1) and (2) simultaneously, \(N_P\) and \(N_{NP}\) are described as
\[ N_P = \frac{\tilde{N}_e - N_e \varepsilon_{UC}}{\varepsilon_{UC}(\varepsilon_P - 1)}, \]
and
\[ N_{NP} = \frac{N_e \varepsilon_P \varepsilon_{UC} - \tilde{N}_e}{\varepsilon_{UC}(\varepsilon_P - 1)}. \]

The fraction of photonic and nonphotonic electrons is then written as
\[ F_P = \frac{\varepsilon_P \varepsilon_{UC} N_P}{\varepsilon_P \varepsilon_{UC} N_P + \varepsilon_{UC} N_{NP}}, \]
and
\[ F_{NP} = \frac{\varepsilon_{UC} N_{NP}}{\varepsilon_P \varepsilon_{UC} N_P + \varepsilon_{UC} N_{NP}}. \]

Figure 3 shows \(F_{NP}\) as a function of \(p_T\) for MB and the indicated four centrality classes. The fraction of photonic electrons \(F_P\) is also shown in the same graph.

D. Invariant yields of heavy-flavor electrons

The invariant yield of heavy-flavor electrons is calculated from the photonic electron yields and the fraction
of heavy-flavor electrons to photonic electrons as
\[
\frac{d^2N_{c+b}}{dp_Tdy} = \frac{d^2N_{e+b}(N_e)}{dp_Tdy} \times \frac{F_{c+b}}{F_P} ,
\]
where \(N_{c+b}^e(N_e)\), \(F_{c+b}\) (\(F_P\)), and \(d^2N_{e+b}/dp_Tdy\) are the yield, fraction, and invariant yield, respectively, of heavy-flavor (photonic) electrons. The photonic electron yield is calculated based on the invariant yields of \(\pi^0\) and \(\eta\) measured by PHENIX [27, 28], using a method which has been demonstrated to give an accurate description of photonic electron yields in the previous heavy-flavor electron measurement [12, 29]. The fractions \(F_{c+b}\) and \(F_P\) are determined by the data-driven method described in the previous section. Note that the efficiency and acceptance cancel out in \(F_{c+b}\) and \(F_P\). The invariant yields of heavy-flavor electrons \((c+b\rightarrow e)\) in MB Au+Au as well as four centrality classes in Au+Au are shown in Fig. 5. The bars and boxes represent statistical and systematic uncertainties which are described in Section IV.

E. DCA\(_T\) distribution of the background

The DCA\(_T\) distribution of misidentified hadrons and mismatched backgrounds are determined by the RICH and VTX swap method as described in Section III C 1. The swap method is data driven and the obtained DCA\(_T\) distribution includes the normalization and resolution effects. Photonic- and nonphotonic-background DCA\(_T\) distributions are determined by the full GEANT-3 simulation of the PHENIX detector. Background sources are generated with the \(p_T\) distribution measured by PHENIX and decay electron tracks are reconstructed and analyzed with the same analysis cuts used to calculate DCA\(_T\). The obtained DCA\(_T\) distributions are fitted with Gaussian functions for photonic, \(J/\psi\), and \(Y\) backgrounds, and Laplace functions for kaon backgrounds to obtain smooth shapes. These DCA\(_T\) distributions are normalized by the factors described in the previous section (III C 1).

The DCA\(_T\) resolution of the data and the Monte-Carlo simulation are compared. The resolution of the DCA\(_T\) distribution is a convolution of the position resolution of the VTX and the beam spot size. The simulation was generated with ideal VTX geometry and a single beam-spot-size value and smeared to correct for differences with the real data caused by irreducible misalignments including the time dependence of the beam spot size during data taking. The smearing is calculated as a function of \(p_T\) by comparing the DCA\(_T\) width of charged hadrons between data and simulation. The smearing is independent of the collision centrality because DCA\(_T\) is measured from the beam center.

Figure 6 shows the smeared and normalized DCA\(_T\) distributions for these background sources. Most of the background sources are primary particles showing up in the DCA\(_T\) distributions as Gaussian shapes. Kaon-decay electrons as well as misidentified and mismatched backgrounds have large DCA\(_T\) tails. Misidentified hadrons contain long-lived hadrons such as \(\Lambda\) particles causing large DCA\(_T\) tails. Mismatch tracks also cause large tails in the DCA\(_T\) distribution because they are formed by hits from different particles.
F. Unfolding

Because the $p_T$ spectra and decay lengths of charm and bottom hadrons are significantly different, simultaneous fits to the $p_T$ and DCA$_T$ distributions of heavy-flavor electrons enable separation of $c\to e$ and $b\to e$ components. However, the $p_T$ and DCA$_T$ template distributions for $c\to e$ and $b\to e$ depend on unmeasured $p_T$ spectra of the parent charm and bottom hadrons. To solve this inverse problem and to measure the hadron yields, the decay of heavy-flavor hadrons into final-state electrons is characterized by using a Bayesian-inference unfolding method that was also used by PHENIX in previous publications [12] [15].

This unfolding procedure is a likelihood-based approach that uses the Markov-chain Monte-Carlo (MCMC) algorithm [30] to sample the parameter space and maximize the joint posterior probability distribution. The response matrix or decay matrix assigns a probability for a hadron at given $p_T^h$ to decay into an electron with $p_T^e$ and DCA$_T$. The yields of charm and bottom hadrons with $17 p_T^h$ bins each within $0 < p_T^h < 20$ GeV/c are set as unfolding parameters.

The PYTHIA6 generator [31] is used to model the decay matrix, which includes charm ($D^0, D^\pm, D_s, \Lambda_c$), and bottom hadrons ($B^0, B^\pm, B_s, \Lambda_b$) from the whole rapidity range decaying into electrons within $|y| < 0.35$. The relative contributions of the charm hadrons and bottom hadrons are modeled by PYTHIA. Thus, the decay matrix has some model dependence which may affect the final results.

In the decay matrix, there are two assumptions. One is that the rapidity distributions of hadrons are not changed in $A+A$ collisions. The BRAHMS collaboration reported [32] that the nuclear modification of pions and protons at $y \approx 3$ is similar to that at midrapidity. The rapidity modification is also less sensitive to the final result because electron contributions from large rapidity to the PHENIX acceptance with $|y| < 0.35$ are small. The second assumption is that the relative contributions of charm (bottom) hadrons are unchanged. The charm hadrons have their own decay lengths which can affect the final results. Charm-baryon enhancement in $Au+Au$ collisions was reported by the STAR collaboration [33]. To study the effect of this, the baryon enhancement for charm and bottom hadrons was tested using a modified decay matrix [34]. Following Ref. [35], the baryon enhancement for charm and bottom is assumed to be the same as that for strange hadrons. The result is that baryon enhancement produces a lower charm-hadron yield and a higher bottom-hadron yield at high $p_T$, but the difference is within the systematic uncertainties discussed in the next section. The test result is not included in the final result.

In each sampling step, a set of hadron yields are se-
the likelihood calculation in the unfolding method. A distribution, but the DCA contributions is mainly contained in the tail of the DCA data are included in the calculation of the log-likelihood. solution is found. Only statistical uncertainties in the predicted by the unfolding procedure. MCMC repeats (\(Y_{5.0 \text{ GeV/c}}\)) and (\(1.0–8.0\) and 1.6–6.0 GeV/c) vectors of measured DCA in the range of 1.0–8.0 and 1.6–6.0 GeV/c, respectively. For the 40%–60% centrality bin, 11 vectors of measured DCA_T in 1.6–5.0 GeV/c are used due to statistical limitations. The \(Y(\theta)\) and \(D(\theta)\) represent the \(p_T\) and DCA_T distribution predicted by the unfolding procedure. MCMC repeats the process through multiple iterations until an optimal solution is found. Only statistical uncertainties in the data are included in the calculation of the log-likelihood.

The analyzing power to separate charm and bottom contributions is mainly contained in the tail of the DCA_T distribution, but the DCA_T distribution has a sharp peak with many measurements at DCA_T = 0, which dominates the likelihood calculation in the unfolding method. A 5% uncertainty is added in quadrature to the statistical uncertainty when a given DCA_T bin has a yield above a threshold that was set to 100.

Without additional information, the unfolding procedure introduces large statistical fluctuations in the unfolded distributions due to negative correlations of adjacent bins. However, the unknown hadron spectra are expected to be relatively smooth. This prior belief of smoothness, \(\pi\), is multiplied with the likelihood to get a posterior distribution \(P\) as

\[
\ln \pi(\theta) = -\alpha^2(|LR_c|^2 + |LR_b|^2),
\]

and

\[
\ln P = \ln \mathcal{L} + \ln \pi(\theta),
\]

where \(L\) denotes a 17 \times 17 matrix of regularization conditions and, \(R_b(R_c)\) is the ratio of the trial bottom (charm) spectra to the prior. The strength of regularization is characterized using a parameter \(\alpha\) that is tuned by repeating the unfolding procedure with several values of \(\alpha\) and selecting the one that gives a maximum of the posterior distribution.

Once the unfolded charm- and bottom-hadron \(p_T\) spectra are obtained, the same response matrices are applied to the heavy-flavor hadron distribution to obtain refolded \(c + b \rightarrow e\) yields. Figure 7 shows the refolded invariant yield of \(c + b \rightarrow e\) compared to the measured data, which is in reasonable agreement with the refolded spectrum. Figure 8 compares the refolded DCA_T distributions to the measured data. The DCA_T distribution is fit with the refolded components within \(|\text{DCA}_T| < 0.1\) cm, and indicates good agreement between the measured and refolded distributions.

IV. SYSTEMATIC UNCERTAINTIES

The systematic uncertainties are independently evaluated for the measured data and the unfolding procedure. Figure 9 shows the contribution of each systematic uncertainty source. The total uncertainty is obtained by adding them in quadrature. Each source of uncertainty is discussed below.

1. Background normalization

Systematic uncertainties associated with modeling of the background processes are estimated from the difference between the nominal measurement and that obtained by repeating the unfolding procedure with systematic variation of the background DCA_T normalization. The background DCA_T template for each source of background is modified independently by \(\pm 1\sigma\) of the nominal value, and the unfolding procedure is repeated with the modified-background DCA_T template. For each background source, the difference between the unfolding result using nominal-background templates and that with a modified-background template is taken as the systematic uncertainty. Estimates of background normalization uncertainty from all the background processes are added.
2. Measured yield of \( c + b \to e \)

The unfolding procedure only considers statistical uncertainty on the measured yield of \( c + b \to e \) in the log-likelihood calculation. The systematic uncertainty on the measured yield of \( c + b \to e \) needs to be accounted for separately. To calculate the systematic uncertainty, an input \( p_T \) spectrum is modified by either kinking or tilting the spectrum. Tilting implies modifying the spectrum by pivoting the nominal spectrum about a given point such that the lowest \( p_T \) point goes up by the systematic uncertainty and the highest \( p_T \) point goes down by the same systematic uncertainty, while the intermediate points are modified with the linear interpolation of the two points. In contrast, kinking implies that the modified spectrum is folded based on the nominal spectrum. The control point for both tilting and kinking is chosen at two points. In contrast, kinking implies that the modified spectrum is folded based on the nominal spectrum.

in quadrature to get a single value of the background normalization uncertainty.
at these points. Once the spectra are modified with this tilting and kinking method, the unfolding procedure is run with 8 modified spectra, and the root mean square of the difference from the nominal result is assigned as a systematic uncertainty.

3. Choice of prior

In the Bayesian approach to unfolding, the prior is chosen to reflect a priori knowledge of model parameters. In this analysis, PYTHIA-based distributions are used to model this initial knowledge. In theory, the optimal distributions obtained through the iterative unfolding procedure should be independent of the choice of the prior. However, residual model dependencies could be present. To account for any uncertainties due to the choice of the prior, the unfolding procedure is repeated with a modified prior, and the difference in the unfolded result from the nominal is assigned as a systematic uncertainty. The modified PYTHIA spectra are obtained by scaling heavy-flavor-hadron yields in PYTHIA with the blast-wave model [37].

4. Regularization hyperparameter

We control the strength of the regularization (spectrum smoothness) with a hyperparameter $\alpha$ of Eq. (9). The uncertainty due to $\alpha$ is determined by changing $\alpha$ by a half unit of the maximum-likelihood value which corresponds to $1\sigma$ deviation. The differences of the unfolded results with these $\alpha$ values are taken as the systematic uncertainty of $\alpha$.

V. RESULTS

A. Invariant yield

The Bayesian unfolding is applied for MB Au+Au collisions as well as for four centrality classes in Au+Au collisions. Figure 10 shows the invariant yields of electrons from charm and bottom hadron decays in Au+Au collisions at $\sqrt{s} = 200$ GeV. The line represents the median of the yield distribution at a given $p_T$ and the band represents the $1\sigma$ limits on the point-to-point correlated uncertainty. These yields are compared with the PHENIX $p+p$ result scaled by the nuclear-overlap function, $T_{AA}$ [18]. Both comparisons of the invariant yields of $c\rightarrow e$ and $b\rightarrow e$ show substantial yield suppression at high $p_T$. The suppression increases at higher $p_T$ and in more-central collisions.

The invariant yields of charm and bottom hadrons are unfolded point-by-point in 17 bins for each centrality class as shown in Fig. 11. The point at each $p_T$ bin is the most likely value of the hadron yields to describe the measured electron yields and DCA$_T$ distributions. Note that the hadron yields are integrated over all rapidity because the decay matrix used in the unfolding method handles all hadron rapidity decaying into electrons in the PHENIX acceptance.

Our unfolded charm-hadron yields have been compared with $D^0$ yields in Au+Au collisions measured by the STAR collaboration [36]. To compare them, PYTHIA is used to calculate the $D^0$ fraction within $|y| < 1$ compared to all charm hadrons for the whole rapidity region. To match the centrality range, the STAR result is scaled by the ratio of the number of binary-collisions. This comparison is shown in Fig. 12. For clarity, we have fit our unfolded $D^0$ yields with the modified Levy function used in Ref. [12]. The ratio of the data to the fit is shown in the bottom panel of Fig. 12. Within uncertainties, the unfolded $D^0$ yield is found to be in qualitative agreement with the $D^0$ yields [36].

B. Nuclear modification factor $R_{AA}$ vs. $p_T$

To compare the yield suppression between charm and bottom quarks, the nuclear-modification factor $R_{AA}$ is
These results extend the $p_T$ coverage down to 1 GeV/c and the systematic bands are reduced by a factor of two. The systematic uncertainty of $R_{AA}^{b\rightarrow e}$ is large at low $p_T$ because of the large uncertainty of $F_{pp}$ at low $p_T$, but the uncertainty of bottom electrons in Au+Au is independent of $p_T$. Significant suppression is seen for electrons from both charm and bottom decays at high $p_T$ at MB and all centrality classes. The nuclear modification is consistent with unity within uncertainties at low $p_T$. Charm electrons show a stronger suppression than bottom electrons for $2 < p_T < 5$ GeV/c in MB and 0%-10%, 10%-20%, 20%-40% centrality classes, whereas charm and bottom suppression are similar at 40%-60%. Note that the prior information used in the unfolding is changed for these centralities. This change can possibly bias the center position of the resulting $c\rightarrow e$ and $b\rightarrow e$ yields. If there is energy loss, then the $p_T$ spectra are shifted to lower $p_T$. Therefore, the resulting $R_{AA}$ is suppressed at high $p_T$, but the yield is slightly enhanced at
The nuclear-modification factors of charm and bottom hadrons is observed in the region of significant difference of the yield suppression between charm and bottom hadrons as shown in Fig. 14. A comparison of the measured yields with the unfolded yield calculated from the STAR collaboration [9] shows that the results for charm and bottom electrons are in good agreement with the STAR measurements within uncertainties. As Fig. 14 shows, our unfolding of the parent charm and bottom hadrons in 0%–80% Au+Au collisions was reported from the STAR collaboration [9].

D. Comparison to theoretical models

Figure 14 shows a comparison of data to three theoretical models: the T-Matrix approach, the SUBATECH model, and the DGLV model. The T-Matrix approach is a calculation assuming formation of a hadronic resonance by a heavy quark in the QGP based on lattice quantum chromodynamics [38]. The SUBATECH model employs a hard thermal loop calculation for the collisional energy loss [40]. Because the DGLV model includes only energy loss and does not include the back reaction in the medium, the curves are only shown for pt > 5 GeV/c. All models expect a quark mass ordering for the energy loss in the QGP medium, as observed in the data. The SUBATECH and DGLV calculations for charm suppression agree with the data. The T-Matrix approach is slightly higher than the data for pt > 3 GeV/c. The measured bottom nuclear modification is larger than the calculations at pt < 4 GeV/c, although the uncertainty in the measurement is large for pt < 2 GeV/c.

VI. SUMMARY AND CONCLUSIONS

This article reported the results of measurements of the separated invariant yields and nuclear-modification factors of charm and bottom hadron-decay electrons in Au+Au collisions at √sNN = 200 GeV at midrapidity. The measurements were performed by the use of a Bayesian unfolding method to extract the invariant yield of parent charm and bottom hadrons from pt and transverse distance of the closest approach DCA_T distributions of decay electrons.

The nuclear-modification factors R_AA have been calculated from the invariant yield in Au+Au and the T_AA scaled yield in p+p. The comparison between R_AA^c/e and R_AA^b/e indicates that charm hadrons are more suppressed than bottom hadrons by at least one standard deviation for 0%-40% central collisions. Quark-mass ordering of suppression is also seen in the R_AA of the parent charm and bottom hadrons, where there is a pattern of R_AA consistent with unity for pt < 1.4 GeV/c for both charm and bottom, charm suppression for 2.6 < pt < 3.0 GeV/c, and suppression of both charm and light quark suppression for pt > 3.0 GeV/c.
FIG. 15. $R_{AA}$ ratio of $b \to c$ to $c \to e$ as a function of $p_T$ for different centrality classes.

FIG. 16. The nuclear modification of charm and bottom hadrons as a function of $p_T$ for different centrality classes. The yellow box at unity is the uncertainty on the total normalization.
FIG. 17. The $R_{AA}$ for $c\rightarrow e$ and $b\rightarrow e$ as a function of $N_{\text{part}}$ in three different $p_T$ ranges. Data points for $c\rightarrow e$ and $b\rightarrow e$ are shifted by -2 and +2 from their respective $N_{\text{part}}$ for clarity.

FIG. 18. Measured $R_{AA}^{c\rightarrow e}$ and $R_{AA}^{b\rightarrow e}$ compared to theoretical-model calculations.

bottom for $p_T > 5.0$ GeV/$c$. These results suggest that charm quarks lose more energy than bottom quarks when crossing the hot and dense medium created in 200 GeV Au+Au collisions in the intermediate-$p_T$ region. The theoretical models used to compare with our data are based on different energy-loss mechanisms and all agree with the mass ordering and the charm suppression for the entire $p_T$ range covered by this measurement. However, the

same models overestimate the bottom-quark suppression in the intermediate $p_T$ region.

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