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The Numerical Diffusion Effect on the CFD Simulation Accuracy of Velocity and Temperature Field for the Application of Sustainable Architecture Methodology

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Abstract: Numerical simulation of fluid flow and heat or mass transfer phenomenon requires numerical solution of Navier–Stokes and energy-conservation equations, together with the continuity equation. The basic problem of solving general transport equations by the Finite Volume Method (FVM) is the exact calculation of the transport quantity. Numerical or false diffusion is a phenomenon of inserting errors in calculations that threaten the accuracy of the computational solution. The paper compares the physical accuracy of the calculation in the Computational Fluid Dynamics (CFD) code in Ansys Fluent using the offered discretization calculation schemes, methods of solving the gradients of the transport quantity on the cell walls, and the influence of the mesh type. The paper offers possibilities on how to reduce numerical errors. In the calculation area, the sharp boundary of two areas with different temperatures is created in the flow direction. The three-dimensional (3D) stationary flow of the fictitious gas is simulated using FVM so that only advective transfer, in terms of momentum and heat, arises. The subject of the study is to determine the level of numerical diffusion (temperature field scattering) and to evaluate the values of the transport quantity (temperature), which are outside the range of specified boundary conditions at variously set calculation parameters.

Keywords: CFD; discretization scheme; numerical diffusion; transport equation

1. Introduction

Aerodynamics deals with the movement of the air and the interaction between airflow and solid objects. Aerodynamics of buildings study the physical problems of airflow effects on buildings and their surroundings. The motion of the air—the wind—affects not only the design of the load-bearing parts of the building structures, but the dimensioning and construction of their non-load-bearing parts. One of the important areas of sustainable architecture is the knowledge of airflow effects on the surrounding objects [1]. The wind significantly affects the energy efficiency of buildings [2], associated with the general phenomenon of air filtration [3] (see Figure 1), the details, elements, and systems of the packaging structures [4].
The aerodynamics of a building examines the effect of the wind on the structure itself [5], the air velocity near the structure [6–10] (see Figure 2), the pressure on the structure [5,11], the turbulence around the building [12], and the influence of meteorological conditions [13]. The mutual grouping of the buildings modifies the airflow, which creates the windy climate in their surroundings [14], and affects the human–wind interaction, human safety, and thermal comfort [15]. By studying the wind movement in relation to the wider topographical units, it is possible to positively regulate the efficiency of the ventilation of the urban units, the scattering of the exhaust fumes, and the formation of snowdrifts around the buildings and the line transport structures [16–18].

![Figure 1. Illustration of air filtration and numerical simulation [3].](image1)

The results of the interaction of air movement and construction can be obtained from real measurements [19], from building scale models in the wind tunnel [20–22], as well as by using computer simulations. Computational Fluid Dynamics (CFD), also called CFD flow analysis, is one of the basic methods in numerical modeling concerning fluid flow, and it is used as a solution to engineering problems in almost all industries [23,24], especially in building construction [4,10].

The numerical solution of the general transport equations in the Ansys Fluent software by the Finite Volume Method (FVM) uses the discretization process, in which the basic problem is the accurate calculation of the transport quantity through the walls of the particular volume and its advective flow across these boundaries [25]. When calculating, it is necessary to count with the occurrence of the so-called “numerical diffusion”, often referred to in literature as “diffusion error” or “numerical viscosity” [26], and with the occurrence of values that are outside the range of the correct solution [27]. This non-physical CFD artifact impairs the accuracy of the discrete solutions of the equations in describing the advection transport of the scalar [28]. It is known that the numerical diffusion occurs mainly in the case where the flow direction is not parallel to the grid walls [29].

However, the optimal states (parallel flow) can only be achieved by calculating straight sections of pipeline without the obstacles using the hexahedral cells [30]. The direction of the flow is always in the general direction with respect to the cell walls (hexahedral, tetrahedral, and polyhedral) in the most flows [31]. When evaluating the advective state, it is necessary to consider the numerical error (numerical diffusion) [32]. This causes considerable problems in the numerical solving of several technical problems, including sustainable architecture.

There are a number of studies improving the numerical solution. Total Variation Diminishing (TVD) schemes have been [33] a widely applied group of monotonicity-preserving advection differencing
schemes for partial differential equations in numerical computational fluid dynamics and heat transfer since the last century. Many scientific teams continue to develop this TVD method. It allows the implementation of the whole spectrum of TVD schemes into unstructured networks, while their exact formulation was restored on structured networks [34]. The authors [35] analyzed the TVD differencing on unstructured three-dimensional meshes, focusing on the non-linearity of TVD differencing and the extrapolation of the virtual upwind node. Furthermore, they proposed a novel monotonicity-preserving correction method for the TVD schemes that significantly reduces the numerical diffusion caused by mesh skewness. The authors [36] analyzed the causes of the numerical errors, in terms of the numerical diffusion and the compression arising from the use of the explicit second-order total variation diminishing schemes in the one-dimensional advection simulation.

The presented work offers possibilities on how to reduce the numerical errors in Ansys Fluent software using the correct calculation settings. It uses the available discretization schemes in the software, together with the available solutions methods of transport quantity gradients. The physical accuracy of the calculations, for the various combination-listed parameters, is monitored on three types of mesh.

The conclusions will recommend suitable variants of calculations and, thus, contribute to better numerical simulations in the field of construction.

2. Method

The three-dimensional stationary virtual gas flow of the computational domain with dimension $1 \times 1 \times 0.25 \text{ m} (x \times y \times z)$ is simulated by the Finite Volume method (FVM). The fictitious gas density is $\rho = 1 \text{ kg·m}^{-3}$. The values of the thermal conductivity $\lambda$ (W·m$^{-1}$·K$^{-1}$) and the dynamic viscosity $\mu$ (Pa·s) of the gas are close to zero. The pressure-velocity coupling algorithm is determined by the segregated SIMPLE method, which is suitable for steady-state calculations [37]. The boundary conditions are set so that the identical vectors enter at the two mutually perpendicular walls with the velocity $v_x$ and $v_y$. One of these walls has the temperature $T_1 = 300 \text{ K}$ and the second $T_2 = 400 \text{ K}$. The pressure outlet is on the two opposite walls (the static pressure $p = 0 \text{ Pa}$). As at the entrance, the outlet temperature is also one wall $T_1 = 300 \text{ K}$ and the second wall $T_2 = 400 \text{ K}$, see Figure 3. Thereby, the sharp boundary of the two domains with the temperature difference $\Delta T = 100 \text{ K}$ is created in the calculation domain. This boundary is in the direction of the flow (in the domain at the angle of 45°). Only the advective transmission, in terms of the momentum and the heat, should occur for the accurate numerical calculation. The diffuse transfer should not occur. The output on the two side opposite walls (in the $xy$ plane) is the zero flow of all quantities across the border (symmetry boundary condition, normal velocity is zero). These two sides of the opposite walls are not shown in Figure 3.

![Figure 3](image-url)
The solution of the problem is independent of the domain dimensions, gas density, and velocity. It was verified on pilot calculations, whereby gradually changing all of these values in the thousands. These test tasks were also performed for porous domain, with a wide range of permeability values corresponding to building materials. The transport quantity does not have to be only the temperature, but also, for example, the concentration of substances. In the presented paper, the size of the calculation area is set so that the calculations did not have the problem with above-standard number of cells and the scattering of the temperature field (numerical error—diffusion) was obvious at the same time. The air density is close to the air density. The velocity is chosen so that the calculations converged in an acceptable time.

The Ansys Fluent software uses the FVM to convert the general transport equations to the system of linear equations that are solved numerically by the Gauss–Seidel iteration method. This solution consists in integrating the equations in each control volume (cell), where the result is the discrete equations presented the flow equilibrium (the conservation laws of the transport quantity Φ in given volume). Its mathematical description for the stationary flow in the integral form is:

$$\int_A \rho \vec{v} \cdot \Phi d\vec{A} = \int_A \Gamma_{\Phi} \nabla \Phi d\vec{A} + \int_V S_{\Phi} dV, \quad (1)$$

where \( \vec{A} \) (m\(^{-1}\)) is the surface vector, \( V \) (m\(^3\)) is the control volume (cell volume), \( \rho \) (kg·m\(^{-3}\)) is the density of the flowing medium, \( \vec{v} \) (m·s\(^{-1}\)) is the velocity vector, \( \Phi \) (K) is the value of the transport quantity (temperature), \( \nabla \Phi \) (K·m\(^{-1}\)) the gradient of the transport quantity \( \Phi \), \( \Gamma_{\Phi} \) is the diffusion coefficient of the transport quantity \( \Phi \) (K·kg·m\(^{-1}\)·s\(^{-1}\)), \( S_{\Phi} \) (K·kg·m\(^{-3}\)·s\(^{-1}\)) is the source term of the quantity \( \Phi \) per unit of the volume.

Equation (1) is applied to all control volumes of the calculation area. Equation (2) is obtained by the discretization of the Equation (1) in the given cell:

$$\sum_{f}^{N_{faces}} \rho_{f} \vec{v}_{f} \Phi_{f} \vec{A}_{f} = \sum_{f}^{N_{faces}} \Gamma_{\Phi} \nabla \Phi_{f} \vec{A}_{f} + S_{\Phi} V, \quad (2)$$

where \( N_{faces} \) is the number of the faces surrounding of the cell, \( \rho_{f} \vec{v}_{f} \vec{A}_{f} \) (kg·s\(^{-1}\)) is the mass flow over the surface \( f \), \( \vec{A}_{f} \) (m\(^2\)) is the surface vector \( f \), \( \Phi_{f} \) (K) is the value of the transport quantity flowing over the surface \( f \) (the face value), \( \nabla \Phi_{f} \) (K·m\(^{-1}\)) is the gradient of the transport quantity \( \Phi \) on the surface \( f \).

The left side in both equations represents the advective transfer of the quantity \( \Phi \), the right side expresses the diffuse transfer and the source term of the transport quantity \( \Phi \) (its decrease or increase). The basic problem in the discretization of the advective term is the exact calculation of the transport quantity on the face of the specific volume \( \Phi_{f} \) and its gradient \( \nabla \Phi_{f} \). The diffusion process affects the transfer of the transport quantity along its gradient in all directions, while the advective transfer pervades only in the direction of the flow. It is very difficult to find the exact discretization computational scheme for the solving of the advective term in the Equation (2). The software Ansys Fluent stores the discrete values of the scalar quantity \( \Phi \) in the center of the cell. The values of the scalar quantity \( \Phi_{f} \) on the cell face are required for the calculation of the advective term in the equations and they are determined by the interpolation from the values in the centers of the adjacent cells. The number of the surrounding cells depends on the type of the grid, but, in most cases, the amount is the same as the number of the faces forming of the interest cell. The discretization “upwind” schemes are used for this process; it means that the value \( \Phi_{f} \) is derived from the value of the next cell in the flow direction. The most upwind schemes require the determination of the transport quantity gradient \( \nabla \Phi \) for their solution. The gradients are necessary for the calculation of the scalar values on the cells faces not only for discretization the advective but also for the diffusion term in the Equation (2).
3. The Parameters Influencing the Accuracy of the Calculation

The level of the physical accuracy of the numerical calculation is influenced by the mesh type, the choice of discretization schemes for the conversion of the general transport equations to the linear equations, and also the choice of the calculating method of the transport quantity gradient $V\Phi$ (here temperatures).

3.1. The Mesh Type and the Mesh Density

Three types of the grids: hexahedral, tetrahedral, and polyhedral are used for solving the problems, see Figure 4. All grid types have double density. The coarse hexahedral and tetrahedral mesh were formed from 25 cells with the length of 1 m at all longitudinal and vertical edges of the domain (z-axis direction), see Figure 5a. The 6 cells per 0.25 m are formed on the domain edges in z-axis direction. The fine hexahedral and tetrahedral mesh were formed from 100 cells per 1 m in the x, y-axis directions, see Figure 5b. The 25 cells per 0.25 m are formed on the domain edges in z-axis direction. The polyhedral mesh was formed directly in the Ansys Fluent from the tetra cells. The six calculation areas with the identical dimensions (Figure 3) and the parameters listed in Table 1 were created.

![Three mesh types and axis scheme on which the transport quantities are evaluated; the coarse mesh: (a) hexahedral; (b) tetrahedral; (c) polyhedral.](image1)

![Two different densities of the tetrahedral mesh: (a) coarse; (b) fine.](image2)

| Mesh Type   | Hexahedral | Tetrahedral | Polyhedral |
|-------------|------------|-------------|------------|
| Values in Thousands | 25 Cells | 100 Cells | 25 Cells | 100 Cells | 25 Cells_tetra | 100 Cells_tetra |
| Cells number | 3.8 | 250 | 28.4 | 1660 | 5.9 | 294 |
| Faces number | 12.2 | 765 | 58.9 | 3355 | 38.8 | 2023 |
| Nodes number | 4.7 | 265 | 5.8 | 294 | 32.9 | 1729 |

3.2. The Discretization Scheme

It is possible that the choice from the five upwind discretization schemes for the given problem. Their brief description and the scheme are in Table 2.
1. Green–Gauss cell-based;  
2. Least Squares cell-based.  

The first two methods use the Green–Gauss theorem to compute the $\nabla \Phi$ at the cell center $c0$:

$$\left(\nabla \Phi\right)_{c0} = \frac{1}{V} \sum_{f} \Phi_{f} \vec{A}_{f}, \quad (3)$$

The face value $\Phi_f$ by default of the Green–Gauss cell-based is taken from the arithmetic average of the values at the neighboring cell centers:

$$\Phi_{f} = \frac{\Phi_{c0} + \Phi_{ci}}{2}. \quad (4)$$

3.3. The Solution of the Transport Quantity Gradients

The gradients are needed, not only for the constructing values of the scalar at the cell faces, but also for computing the secondary diffusion terms and the velocity derivatives. The gradient $\nabla \Phi$ of a given the variable $\Phi$ is used to discretization of the advection and the diffusion terms in the flow conservation equations. The gradients are computed in Ansys Fluent, according to the three following methods:

1. Green–Gauss cell-based;  
2. Green–Gauss node-based;  
3. Least Squares cell-based.

First-order upwind scheme is based on the assumption that the value of the quantity in the cell center corresponds to the average value in the whole control volume and the face value $\Phi_f$ is set equal to the cell-center value of $\Phi$ in the upstream cell. The first-order upwind scheme is not depended on the gradient $\nabla \Phi$. Power law scheme is based on the analytical solution the one-dimensional advection-diffusion equation. The face value $\Phi_f$ is determined from the exponential profile by using the values of the cell in their center. The exponential profile is depended on the Peclet number $Pe$ (ratio of the convection heat flow (advection) and the heat flow by the mechanism of the convection (diffusion)). The solution is the same with the first-order upwind scheme for $|Pe| \geq 10$. Second-order upwind scheme: the face value $\Phi_f$ is determined from the cell values in the two cells upstream of the face. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. This is more accurate than the first-order upwind scheme, but in the regions with the strong gradients, it can result in the face values that are outside of the range of the correct cell values. Quadratic Upwind Interpolation for Convective Kinetics (QUICK) scheme. The quadratic curve is fitted with two upstream nodes and one downstream node. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. This is a very accurate scheme, but it can lead to stability problems in the calculation in the regions with strong gradients. QUICK scheme, documented in [37], is mainly suitable for the structured hexahedral meshes, but it can be used for the unstructured or the hybrid meshes. Third-order Monotone Upstream-centered Scheme for Conservation Laws (MUSCL). This third-order convection scheme was created from the original MUSCL [28], by mixing the central differentiation scheme and the second-order winding scheme. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. It is usable for all grid types.

### Table 2. The discretization schemes for the adventive flow calculation.

| Flow Direction | Description of Discretization Schemes |
|----------------|--------------------------------------|
|               | First-order upwind scheme is based on the assumption that the value of the quantity in the cell center corresponds to the average value in the whole control volume and the face value $\Phi_f$ is set equal to the cell-center value of $\Phi$ in the upstream cell. The first-order upwind scheme is not depended on the gradient $\nabla \Phi$. Power law scheme is based on the analytical solution the one-dimensional advection-diffusion equation. The face value $\Phi_f$ is determined from the exponential profile by using the values of the cell in their center. The exponential profile is depended on the Peclet number $Pe$ (ratio of the convection heat flow (advection) and the heat flow by the mechanism of the convection (diffusion)). The solution is the same with the first-order upwind scheme for $|Pe| \geq 10$. Second-order upwind scheme: the face value $\Phi_f$ is determined from the cell values in the two cells upstream of the face. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. This is more accurate than the first-order upwind scheme, but in the regions with the strong gradients, it can result in the face values that are outside of the range of the correct cell values. Quadratic Upwind Interpolation for Convective Kinetics (QUICK) scheme. The quadratic curve is fitted with two upstream nodes and one downstream node. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. This is a very accurate scheme, but it can lead to stability problems in the calculation in the regions with strong gradients. QUICK scheme, documented in [37], is mainly suitable for the structured hexahedral meshes, but it can be used for the unstructured or the hybrid meshes. Third-order Monotone Upstream-centered Scheme for Conservation Laws (MUSCL). This third-order convection scheme was created from the original MUSCL [28], by mixing the central differentiation scheme and the second-order winding scheme. This scheme requires the determination of the gradient $\nabla \Phi$ in each cell. It is usable for all grid types. |
4. Results

The influence of the setting combination the above parameters on the accuracy of the calculation is tested in this paper. The level of the temperature field scattering (numerical diffusion) is compared to the original sharp boundary of two areas with the temperature difference \( \Delta T = 100 \text{ K} \). The study also monitors in which cases the temperature values appear outside the range of the specified boundary conditions, i.e., outside the range \( T \in (300 \text{ K}, 400 \text{ K}) \).

4.1. Evaluation the Mesh Density and the Mesh Type on the Numerical Diffusion

It is generally known that the mesh density has a significant effect on the magnitude of the numerical diffusion. Figure 6 shows the temperature fields in the median plane of the calculation area \((\text{plane } z = 0.125 \text{ m}, \text{see Figure 3})\) calculated using the hexahedral meshes, the coarse also the fine grids. The difference in the temperature scattering with the mesh density of 25 cells/m versus the mesh density of 100 cells/m is shown. Figure 6a,b presents the results of the solutions using the first-order upwind scheme and Figure 6c,d using the second-order upwind scheme. The similar effect has the grid density on the numerical diffusion using the first-order upwind scheme for the tetrahedral and polyhedral mesh types. Using the second-order upwind, QUICK, and the third-order MUSCL discretization schemes, the scatterings of the temperature fields and their changes (by changing of the grid density) are smaller in all meshes, but there are problems with the temperature values outside the range of the correct solution (more Section 4.4).

![Figure 6](image_url)

**Figure 6.** Hexahedral elements, influence of the mesh density on the temperature field scattering: (a) 25 cells/meter, first-order; (b) 100 cells/meter, first-order; (c) 25 cells/meter, second-order; (d) 100 cells/meter, second-order.

The grid type also has influence on the numerical diffusion of the transport quantity, although not as significant as its density. The comparison of the temperature fields scatterings for all three types of the coarse grids (25 cells/m) for the identically selected calculation scheme (second-order upwind) and the method of the solution of the transport quantity gradients (Green–Gauss node-based) is shown in Figure 7. Figure 7a–c document the temperature field from the Ansys Fluent software and Figure 7d the temperature diagram in the horizontal axis of the calculation area \((y = 0.5 \text{ m}, z = 0.125 \text{ m})\). As it
can be seen from Figure 7, the smallest scattering is achieved using the tetrahedral elements using the coarse mesh and the described calculation setting. Contrariwise, the biggest numerical diffusion arises using the hexahedral elements. The ideal variant (“ideal”) is the illustrative fictitious case with the zero numerical diffusion in Figure 7d.

Figure 7. Coarse mesh, 25 cells/meter, second-order, influence of the grid type on the temperature field scattering: (a) hexahedral; (b) tetrahedral; (c) polyhedral; (d) the temperature diagram in the direction of horizontal axis ($y = 0.5 \text{ m}, z = 0.125 \text{ m}$). The legend is identical with legend in Figure 6.

The temperature fields using the fine mesh with the unchanged calculation parameters are in Figure 8. It is obvious that the differences in the individual results are smaller. The tetrahedral mesh still achieves the most accurate result.

Figure 8. Fine mesh, 100 cells/meter, second-order, influence of the grid type on the temperature field scattering: (a) hexahedral; (b) tetrahedral; (c) polyhedral; (d) the temperature diagram in the direction of horizontal axis ($y = 0.5 \text{ m}, z = 0.125 \text{ m}$). The legend is identical with legend in Figure 6.

However, it is important to remember that the overall evaluation of the mesh type is necessary to perform in parallel with the choice of the discretization scheme and the method of calculating the gradient of the transport quantity on the control volume face (see next chapter).

4.2. Evaluation of the Discretization Schemes in the Numerical Diffusion

The discretization schemes listed in Section 3.2, except the power law scheme, are tested. The solution of the power law scheme is identical with the first-order upwind scheme in this type of the problem ($|\text{Pe}| > 10$).

Figure 9 shows the temperature diagrams for all upwind schemes using the hexahedral mesh. The Green–Gauss node-based method was chosen for the transport quantity gradients in all cases presented here. The results using the coarse and fine grids are compared here. The results of the first-order upwind scheme are significantly diffusive, yet the differences are slight in other cases. The smallest temperature field scatterings in this case is shown by the QUICK scheme using the fine mesh.
This also applies to the polyhedral mesh. It will be discussed in more detail in the following chapters.

The Green–Gauss node-based method was chosen for the transport quantity gradients in all cases evaluated in the next section.

The higher-order discretization schemes give the small mutual differences, but the results are more pronounced for the different choice of the methods of the transport quantity gradients. This will be evaluated in the next section.

Figure 9. Influence of the discretization scheme choice on the temperature field scattering, hexahedral elements, node-based method for the transport quantity gradients, \( y = 0.5 \text{ m}, z = 0.125 \text{ m} \): (a) 25 points/meter; (b) 100 points/meter.

Figure 10 shows the temperature diagrams only for the fine tetrahedral mesh (all upwind schemes) but the record on the horizontal axis in the higher layer is also added (\( y = 0.9 \text{ m}, z = 0.125 \text{ m} \)). The Green–Gauss node-based method was chosen for the transport quantity gradients in all cases presented here. It is in this case, when the different temperatures limit is at the greater distance from the entrance to the calculation area (\( x = 0.9 \text{ m} \)). It is evident from the graphs that the mutual differences in the results between the selected schemes remain very similar along the entire length of the sharp boundary of the different temperatures. The numerical diffusion increases slightly at the greater distance from the entrance to the area (\( y = 0.9 \text{ m} \)). The results give only slight differences using the tetrahedral mesh except of the first-order upwind scheme. The smallest temperature field scattering is now shown the third-order MUSCL, and this positivity is slightly highlighted at the great distance. This also applies to the polyhedral mesh. It will be discussed in more detail in the following chapters.

Figure 10. Influence of the discretization scheme choice on the temperature field scattering, tetrahedral elements, node-based method for the transport quantity gradients, 100 points/meter, \( y = 0.5 \text{ m}, \) \( z = 0.125 \text{ m} \): (a) \( y = 0.5 \text{ m} \); (b) \( y = 0.9 \text{ m} \).

It is apparent that the calculation in all cases using the first-order upwind scheme creates a significantly larger scattering of the transport quantity in comparing with the other schemes. Although the higher-order discretization schemes give the small mutual differences, but the results are more pronounced for the different choice of the methods of the transport quantity gradients. This will be evaluated in the next section.
4.3. Evaluation of the Transport Quantity Gradients on the Numerical Diffusion

The influence of the method choice for the transport quantity gradients solving of the numerical diffusion is presented here for all fine mesh types (100 cells/meter). The temperature change record for \( y = 0.9; z = 0.12 \) m is shown in Figures 11–15. The first-order upwind scheme does not depend on the gradient of the transport quantity \( \nabla \Phi \), as Table 2 was shown. The temperature field scattering is significant (it was also shown in Section 4.2.) and it varies only due to the mesh type change (Figure 11).

**Figure 11.** First-order upwind scheme: influence of the method choice for the solving of the transport quantity gradients and the mesh type on the numerical diffusion; 100 cells/m; \( y = 0.9; z = 0.125 \) m.

**Figure 12.** Hexahedral mesh: influence of the method choice for the solving of the transport quantity gradients and the mesh type on the numerical diffusion; 100 cells/m; \( y = 0.9; z = 0.125 \) m.

**Figure 13.** Tetrahedral mesh: influence of the method choice for the solving of the transport quantity gradients and the mesh type on the numerical diffusion; 100 cells/m; \( y = 0.9; z = 0.125 \) m.
MUSCL. The Green–Gauss node-based method shows significantly larger scattering of the temperature gradients compared to the method for solving transport quantity gradients, and the influence of the choice of the methods for solving the transport quantity gradient is small in the case of the diffusivity. QUICK schemes show the same results, where the temperature field scattering is larger than the least diffusivity.

**Figure 14.** Percentage values of the error from the ideal sharp limit of the temperature field in the immediate vicinity of this limit: (a) combination of calculation parameters on specific meshes; (b) combination of calculation parameters for a specific upwind scheme; 100 cells/m; \( y = 0.9 \); \( z = 0.125 \) m.

![Figure 14](image)

**Figure 15.** Polyhedral mesh: influence of the method choice for the solving of the transport quantity gradients and the mesh type on the numerical diffusion; 100 cells/m; \( y = 0.9 \); \( z = 0.125 \) m.

![Figure 15](image)

The results of the other discretization schemes prove the certain dependence from the choice of the method for the solving transport quantity gradients and they differ according to the mesh type.

Hexahedral mesh (Figures 12 and 14): the choice of the method for the solving transport quantity gradients affects the results in the combination using the Second-order upwind and the third-order MUSCL. The Green–Gauss node-based method shows significantly larger scattering of the temperature...
field in comparing with the other two methods. The greatest numerical diffusion arises using the second-order upwind scheme and all methods for solving the transport quantity gradients. The highest diffusivity using the hexahedral mesh (second-order upwind scheme and Green–Gauss node-based method) is comparable to the same calculation using the tetrahedral mesh (Figure 13). The calculation using the QUICK scheme, using the hexahedral mesh, is one of the most accurate, and the choice method for solving the transport quantity gradients in this case will not affect the results.

Tetrahedral mesh (Figures 13 and 14): the method for solving the transport quantity gradient using the tetrahedral mesh affects the results for all discretization schemes, and the differences are more pronounced than used the hexahedral mesh. In the case of the Green–Gauss cell-based method choice, the numerical calculations have almost identical results in all discretization schemes and their diffusivity is the most pronounced. Conversely, the smallest scattering of the temperature field is achieved using the third-order MUSCL with the Green–Gauss node-based method option. The second-order upwind and the QUICK schemes with options, the Green–Gauss node-based, and the least squares cell-based methods, using this grid show good, almost identical results, in terms of the diffusivity on their accuracy, and is comparable to the QUICK hexahedral mesh scheme.

The percentage expression of the of the transport quantity error value from the ideal sharp limit in the line $y = 0.9$ m is shown in Figure 14. The area in the immediate vicinity of this limit $x \in (0.88$ m, 0.92 m) is not evaluated. The reason is the discontinuous function of ideal values. Figure 14a (left) presents the effect of different combinations of the calculation parameters on the specific meshes. The percentage expression of the error from the ideal value is in accordance with the real temperature diagram in Figure 12, Figure 13, or Figure 15. Figure 14b (right) shows the effect of the mesh type and the method for the solving of the transport quantity gradient on the results of the chosen upwind scheme.

Polyhedral mesh (Figures 14 and 15): the numerical diffusion using the polyhedral mesh is not affected by the choice of the methods for the solving of the transport quantity gradient. The small differences arise only by changing of the discretization scheme. The second-order upwind and the QUICK schemes show the same results, where the temperature field scattering is larger than the solving used the third-order MUSCL. Compared to other meshes, the results show the average diffusivity.

4.4. Values of the Transport Quantities outside the Range of the Input Parameters

The choices of the discretization scheme and the method for the solving of the transport quantity gradient affect to the formation of the transport quantity values outside the range of the input parameters; it is also affected in the accuracy of the numerical calculations.

The lowest temperature deflections occur using of the hexahedral mesh. Their values outside the boundary conditions $T \in (300$ K, 400 K) are documented in Figure 16. The results differ significantly in comparing with the results using the other mesh; therefore, the scale in this case is ten times smaller than the following images. The highest deflections occurred using the dense mesh (100 cells/m) using the third-order MUSCL with the Green–Gauss cell-based method. The frequency of these deflections in the median plane of the calculation area (plane $z = 0.125$ m, see Figure 3) is shown in Figure 17a. Although the frequency is relatively high, these deflections can be considered negligible due to their minimum values. Figure 17b shows the frequency of the deflections using the Second-order upwind scheme with the Green–Gauss node-based; this shows the second highest values using the hexahedral mesh.
Figure 16. Hexahedral mesh: the extreme values of the transport quantities outside the range of the correct solution: (a) coarse mesh; (b) fine mesh.

Figure 17. Frequency of the transport quantity deflections outside the range of input parameters (white field), fine mesh: (a) hexahedral, third-order MUSCL; (b) hexahedral, second-order; (c) tetrahedral; (d) polyhedral.

The significant extreme deflections of the specified temperature field values for solving the transport quantity gradient using the tetrahedral mesh occur, the third-order MUSCL for all methods. It is markedly for the coarse mesh, see Figure 18a. The deflection values using the fine mesh are in Figure 18b. The first and second-order upwind and the QUICK schemes have the targeted 10 × smaller scale (identical with the hexahedral), because the temperature values outside the range $T \in (300 \text{ K}, 400 \text{ K})$ are in order of the magnitude lower (maximum $\pm 0.4 \text{ K}$) than using the third-order MUSCL. This scheme has the scale identical to the coarse mesh.

Figure 18. Tetrahedral mesh: the extreme values of the transport quantities outside the range of the correct solution: (a) coarse mesh; (b) fine mesh.
The absolute highest deflections of the temperature values occur for the calculation using the Green–Gauss node-based method, both the fine and the coarse mesh, and this is the highest value exceedance of all variants of \( T = 400 \) K, see Figure 18. The frequency of the deflections for this case is in Figure 17c.

Using the polyhedral mesh gives almost zero exceeding values in the range of \( T \in (300 \text{ K}, 400 \text{ K}) \) except for the third-order MUSCL. This applies to all methods for solving the transport quantity gradient; see Figure 19. The highest deflections occur for the calculation using the Green–Gauss node-based method. Figure 17d shows the frequency of the deflections.

![Figure 19. Polyhedral mesh: the extreme values of the transport quantities outside the range of the correct solution: (a) coarse mesh; (b) fine mesh.](image)

5. Discussion

5.1. Mesh Type

Hexahedral mesh:
- Using the correct combination of the calculation parameters achieve the most accurate results of all tested tasks, but the results are diffusive with incorrect settings (for more see Section 5.2).
- The lowest deflection of the entered values of the transport quantity \( \Phi \) occur on this mesh.
- The calculations are less sensitive to the choice of methods for solving the transport quantity gradient than using the tetrahedral mesh, unfortunately, in many cases, it is not possible to create the hexahedral cells for complex geometries separately.

Tetrahedral mesh:
- The disadvantage is the large number of cells and, thus, the greater complexity of calculations.
- The sensitivity to the choice of calculation parameters is high, but with the correct combination, can achieve good results (for more see Section 5.2).

Polyhedral mesh:
- In many cases, it is recommended for great savings in the number of cells and, thus, less difficulty in the calculations.
- The accuracy of the solutions is average to below average in this submitted study (see Section 5.2 for more information).

5.2. Discretization Scheme and the Method for Solving the Transport Quantity Gradients

First-order upwind scheme:
- Produces very diffusive results, but it is easy to implement and its calculations are very stable.
• This scheme is convenient for starting calculations.

Second-order upwind scheme:
• It is more accurate than the first-order upwind scheme, but it is generally stated that it can lead to the values—that they are outside the range of the input in the regions with the strong gradients [38]. It is reflected in both the hexahedral and the tetrahedral mesh, but the deflections of the values are very low (see Figures 16 and 18), and the frequency of the occurrence does not exceed the other cases (see Figure 17b).
• This scheme achieves the weakest results among the higher order schemes using the hexahedral mesh.
• Conversely, the solution using the tetrahedral mesh with the choice of the node-based and the least methods, together with the QUICK scheme, is relatively accurate, and comparable to the most accurate, using the hexahedral mesh (see Figures 12–14).

QUICK scheme:
• The scheme, stated in [37], is suitable mainly for the structured hexahedral meshes, but it can be used for the unstructured or hybrid meshes.
• Using the hexahedral mesh, this scheme presents the most accurate results of all tested variants, regardless of the choice of the method for solving the transport quantity gradient.
• The QUICK scheme, using the tetrahedral mesh, gives the results in terms of the size of the numerical diffusion comparable to the hexahedral mesh with the combination the Green–Gauss node-based or the least squares cell-based methods (Figures 12–14), but there are slightly higher values of the temperature field value deflections. (Figures 16 and 18).
• The combination of the QUICK scheme with the Green–Gauss cell-based method for solving the transport quantity gradient is not suitable for the tetrahedral mesh; the results are very diffusive.

Third-order MUSCL:
• The scheme has the potential to improve the spatial accuracy for all types of grids by reducing the numerical diffusion and it is available for all transport equations. This is confirmed only by the numerical calculations using the tetrahedral mesh in combination with the Green–Gauss node-based method. However, the occurrence of the values outside the correct solution is high (see Figure 13, Figure 14 or Figure 18), and the high deflections are also for the other methods.
• This scheme shows the high deflections of the values of the transport quantity for the tetrahedral and the polyhedral meshes in all methods for solving the transport quantity gradient (see Figures 18 and 19).

The recommended combinations of the calculation parameters are in Table 3. The unrecommended settings are listed in Table 4.

Table 3. Recommended combinations of the calculation parameters settings for three mesh types.

| Mesh Type   | Discretization Scheme | Method for Solving Transport Quantity Gradient | Numerical Diffusion | Out Range Values |
|-------------|-----------------------|-----------------------------------------------|--------------------|------------------|
| Hexahedral  | QUICK scheme          | Method does not affect Green–Gauss node-based, or least squares cell-based | Lowest of all variants | Significantly low |
| Tetrahedral | Second-order and QUICK schemes | Method does not affect | Small | Low |
| Polyhedral  | Second-order and QUICK schemes | Method does not affect | United | Low |
|             | Third-order           | Method does not affect | Average | High |
6. Conclusions

The presented work compares the physical accuracy of the calculation in the CFD code in the Ansys Fluent software using the offered discretization calculation schemes, the methods of the transport quantity gradients solving on the cell faces, and the influence of the mesh type. The sharp boundary of two areas with the different temperatures is created in the direction of the flow direction in the calculation area. The FVM simulates the 3D stationary flow of the fictitious gas so that only the advective transfer in the terms of the momentum and the heat arises. Ideally, the diffuse transmission should not occur. The level of the scattering of the temperature field (numerical diffusion) against the original sharp boundary of the two areas is monitored and also in which cases the values of the transport quantity (temperature) appear outside the range of the specified boundary conditions, i.e., outside the $T \in \text{range (300 K, 400 K)}$. The frequencies of the deflections and the value deflections from the correct solution are evaluated.

The article offers the options for reducing of the numerical errors by setting the correct combination of the calculation parameters. The recommended combinations of the calculation parameters settings for the numerical modeling of the airflow effect on the buildings, including the partial results, are described in detail in the Results section. Their global summary is commented in the Discussion section.

The results of the presented study contribute to the development of the methodology for the numerical studies focused on the sustainable architecture. The conclusions will be used in solving specific problems of construction engineering practices, for example, in solving the velocity of substances in the porous domain of building materials and soils.

Final practical summary:

- The coarse mesh is to be clearly more accurate.
- The first-order upwind scheme does not depend on the choice of the methods for the solving of the transport quantity gradient, it produces the very diffusive results, but the calculation is stable, and it is suitable for starting calculations that are more complex. When calculating with the first-order upwind scheme, the values of the transport quantity $\Phi$ do not occur outside the input range.
- The QUICK scheme shows the best results with the low diffusivity, even with the low values $\Phi$ outside the input range. The effect of the choice of the methods for solving the transport quantity gradient is manifested only on the tetrahedral mesh.
- Although the third-order MUSCL is able to calculate the acceptable diffusivity, the values $\Phi$ outside the input range are significantly high compared to other discretization schemes.
- The Green–Gauss cell-based method for the solving the transport quantity gradient is not suitable for the tetrahedral mesh; it shows the diffusive results for all discretization schemes except the first-order upwind.
- The Green–Gauss node-based method for the solving of the transport quantity gradient is not suitable for the hexahedral mesh using the second-order upwind and the third-order MUSCL. It shows the diffusive results with these schemes.
- The advantage of the polyhedral mesh with the low number of cells and, thus, less computational complexity, is negatively balanced by the higher diffusivity in all discretization schemes. The effect of the method for solving the transport quantity gradient option has no effect on the results on this mesh.

| Mesh Type | Discretization Scheme | Explanation |
|-----------|-----------------------|-------------|
| Hexahedral | Second-order scheme    | High diffusion, the largest for Green–Gauss node-based choice, values outside the input range are low; Figure 12, Figure 14, and Figure 16. |
|           | Third-order scheme     | High diffusion for Green–Gauss node-based choice, values outside the input range significantly high, Figure 12, Figure 14, and Figure 16. |
| Tetrahedral | All schemes           | Height diffusion for Green–Gauss cell-based choice, Figures 13 and 14. |
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