A new Rubidium - Bismuth polyphosphate RbBi(PO$_3$)$_4$: Growth, X-ray single crystal and vibrational study

Khaled JAOUADI*, Tahar MHIRI, Nabil ZOUARI

Laboratoire physico-chimie de l’état solide, Faculté des Sciences de Sfax, BP 1171, 3038 Sfax, Tunisie

khaledjaouadi@yahoo.fr

Laboratoire physico-chimie de l’état solide, Faculté des Sciences de Sfax, BP 1171, 3038 Sfax, Tunisie

taharmhiri@yahoo.fr

Laboratoire physico-chimie de l’état solide, Faculté des Sciences de Sfax, BP 1171, 3038 Sfax, Tunisie

bizrirl@yahoo.fr

ABSTRACT

Solid-solution studies in the ternary Rb$_2$O – Bi$_2$O$_3$ – P$_2$O$_5$ system, carried out in a search for inorganic materials have a considerable interest mainly for their optical properties, specifically in laser technology, yielded the new compound RbBi(PO$_3$)$_4$. Single-crystal X-ray measurement revealed that RbBi(PO$_3$)$_4$ crystallizes in space group P2$_1$/c with a structural type IV and has lattice parameters a = 10.430 Å, b = 8.984 Å, c = 12.967 Å, β = 126.1°, Z = 4 and V = 981.6 Å$^3$. The all eighteen atoms were located in the asymmetric unit. Refinement using anisotropic temperature factors for all atoms yielded weighted residuals based on F and F$^2$ values, respectively, of R$_1$ = 0.0131 and WRF$_2$ = 0.0252 for all observed reflections. The atomic arrangement can be described as a long chain polyphosphate organization, helical ribbons (PO$_3$)$_n$. Two types of infinite chains, with a period of eight PO$_4$ tetrahedra run along the longest unit-cell directions. Infrared and Raman spectra at room temperature, were investigated, show clearly some characteristics bands of infinite chains structure of PO$_4$ tetrahedra linked by a bridge oxygen.

Indexing terms/Keywords

Inorganic materials; Crystal structure; X-Ray diffraction; IR spectroscopy; Raman spectroscopy.
1. INTRODUCTION

The structure investigation of the compound RbBi(PO$_3$)$_4$ was performed as part of a research program in condensed phosphates with general formula M$^+$M$^{III}(PO$_3$)$_4$ (where M$^+$ is a monovalent cation: Li, Na, Ag, K … and M$^{III}$ is a trivalent cation: Nd, La, Sm, Ce, Y…). The common chemical features of these polyphosphates report that are relatively stable under normal conditions of temperature and humidity [1-7]. These compounds can be kept for many years in a perfect state of crystallinity; they are not water soluble as may be inferred from their estimated molecular weights and they all produce glasses when heated to their melting points [8]. The literature dealing with these compounds was rather confusing for a long time, but it is currently well established that the M$^+$M$^{III}(PO$_3$)$_4$ compounds can be classified into seven different structure types, which are usually denoted by the roman numerals I to VII. This nomenclature, first proposed by Palkina and al [9] is to-day generally accepted. In addition, many of these compounds are isotypic and some of them are polymorphic. Only the two polyphosphates KBi(PO$_3$)$_4$ (type IV) and NaBi(PO$_3$)$_4$ (type II) have been elaborated in the ternary M$^+$O – Bi$^+$O$_3$ – P$_2$O$_5$ system and their structures were well discussed by Jaouadi and al [10, 11], and up to now, the syntheses and the crystal structure of the other types of polyphosphates existing in this ternary system have been unknown.

Our attempt to prepare new single crystals, in the ternary P$_2$O$_5$ – Rb$_2$O – Bi$^+$O$_3$ system, from phosphoric acid, bismuth oxide and rubidium carbonate was successful. In fact, this study resulted in a new polyphosphate RbBi(PO$_3$)$_4$ (type IV), whose chemical preparation and crystal structure are presented here. In addition, the titled compound has been characterized by IR and Raman vibrational spectroscopy.

2. EXPERIMENTAL

2.1. Synthesis and characterization

Single crystal of RbBi(PO$_3$)$_4$ was prepared by a flux method. At room temperature, 2.8 g of Rb$_2$CO$_3$ and 0.52 g of Bi$_2$O$_3$ were slowly added to 2.5 ml of phosphoric acid H$_3$PO$_4$ (85 %). The mixture was then slowly heated to 623 K and kept in this temperature for 24 hours. A few days later of decreasing temperature by 40°C/day to reach 323 K, a colorless, transparent and parallelepiped crystals were separated from the excess phosphoric acid by washing the product in boiling water. Subsequently, a second washing with nitric acid is necessary to eliminate the remaining oxide Bi$_2$O$_3$. Several preparations based on the temperature decreasing speed were necessary to obtain single crystals of dimensions 0.16 × 0.18 × 0.08 mm$^3$ suitable for X-ray study (Figure 1).

![Figure 1: Photograph of single crystal of RbBi(PO$_3$)$_4$ grown by the flux method](image-url)

This compound is stable in air and its formula is determined by chemical analysis (Table 1) and confirmed by refinement of the crystal structure. In fact, the single crystals already formed correspond to the composition RbBi(PO$_3$)$_4$. It is noted that many preparation with respect to this stoichiometry always led to the same density of crystals (d$_{mes}$ = 4.128). Infrared absorption spectra of suspensions of crystalline powders in KBr were recorded on a Perkin-Elmer 753 spectrophotometer in the 400 – 1500 cm$^{-1}$ range. Raman spectra of polycrystalline samples scaled in glass tubes were performed by employing an RTI DILOR triple monochromated apparatus using the 514.5 nm line of a spectra-physics argon ion laser.
Table 1: Results of chemical analysis for RbBi(PO₃)₄

|          | P (%) | Rb (%) | Bi (%) |
|----------|-------|--------|--------|
| calculated | 20.25 | 14.00  | 34.24  |
| experimental | 19.42⁻| 13.92ᵇ| 33.83ᶜ|

⁻ Determined by spectrophotometry.
ᵇ Determined by atomic absorption.
ᶜ Determined by ICP method.

2.2. X-ray diffraction and data collection

Single-crystal X-ray intensity data were collected at room temperature from an as-synthesized specimen measuring 0.16 × 0.18 × 0.08 mm³ in size. Data were obtained in Mo-Kα radiation (λ = 0.71073 Å) using an Enraf-Nonius Kappa CCD diffractometer. Refinement of the lattice parameters, using the locations of twenty five peaks, revealed RbBi(PO₃)₄ to be monoclinic with lattice parameters a = 10.430 (5) Å, b = 8.984 (4) Å, c = 12.967 (4) Å and β = 126.1 (3)°. The raw intensity data were corrected for Lorenz and polarizing effects before proceeding to the refinement of the structure. An empirical absorption correction was performed by using psi-scan method [12]. Atomic scattering factors were taken from the International Tables for X-ray crystallography [13]. 2429 reflections were collected in the whole Ewald sphere for 2.42 ≤ θ ≤ 28.68; -13 ≤ h ≤ 11; 0 ≤ k ≤ 11; 0 ≤ l ≤ 17. The overage of the equivalent reflections with I/σ(I) > 2, with respect to the P2₁/c symmetry, gave a final set of 2254 unique observations. The intensities of two standard reflections (3 2 4 and 3 2 4) were periodically recorded to check the stability of the data acquisition. The remaining data collection parameters, along with some crystallographic data and parameters related to the refinement, are provided in Table 2.

Bismuth and rubidium atom positions were located using SHELXS–97 program [14], whereas phosphorus and oxygen atom positions were deduced from Fourier-difference map during the refinement of the structure with an adapted version SHELXL–97 program [15]. There are four formula units in the unit cell and all the atoms are in general positions. The structural graphics were created with ATOMS [16]. The final cycle of refinement leads to the final discrepancy factors R₁ = 0.0131 and WR₂ = 0.0252. The residual electron density ranged between -1.350 and 1.170 e/Å³, near the Bismuth atom. The final fractional atomic coordinates and equivalent isotropic thermal parameters are given in Tables 3 and 4.

3. RESULTS AND DISCUSSION

3.1. Description of the structure

Views of the structure of RbBi(PO₃)₄, projected along the b- and a- axes, are illustrated in figures 2 and 3 respectively. As a result of our investigations on polyphosphates, RbBi(PO₃)₄ was shown to be isostructural with KBi(PO₃)₄ [10], KGD(PO₃)₄ [17] and CsGD(PO₃)₄ [18].

Figure 2: The RbBi(PO₃)₄ structure projected along the b axis

From a general point of view, this phosphate could be described as a long chain polyphosphate containing alternating (PO₃)ₙ chains and (M⁺⁻, M⁺⁺) cations along the [0 1 1] direction. One can assume that this atomic arrangement is characteristic of this family of polyphosphates [10, 17, 18]. As illustrated in figure 2, the basic structural units are helical ribbons (PO₃)ₙ, formed by corner-sharing of PO₄ tetrahedra. The ribbons (two per unit cell) run along the longest unit-cell directions, with a period of eight tetrahedral. Every two chains are symmetrical by a twofold axis (Figure 2). These chains are joined to each other by BiO₈ dodecahedra, driving to a tree-dimensional structure, with the Rb⁺ cations located in framework tunnels (Figure 3).
Table 2: Main crystallographic features, X-ray diffraction data collection parameters and final results for RbBi(PO$_3$)$_4$

| I - Crystal Data |  |  |
|------------------|------------------|------------------|
| Formula          | RbBi(PO$_3$)$_4$ | 610.33           |
| Formula weight (g/mol) | 610.33           |                  |
| Crystal system: Monoclinic | 610.33           |                  |
| a = 10.430 (5) Å  | Space group: P2$_1$/c |                  |
| b = 8.984 (4) Å  | β = 126.1 (3)°   |                  |
| c = 12.967 (4) Å | Z = 4            |                  |
| d$_{cal}$ = 4.130 | V = 981.6 (7) Å$^3$ |                  |
| Habit            | μ = 8.606 mm$^{-1}$ |                  |
| Crystal shape    | colorless        |                  |
| Crystal size     | parallelepiped   |                  |
|  | (0.16 × 0.18 × 0.08) mm$^3$ |                  |
| II - Intensity Measurements | 293 (2) K |                  |
| Temperature:     | Enraf-Nonius Kappa CCD |                  |
| Diffractometer:  | λ(Mo-K$_α$) = 0.71073 Å |                  |
| Radiation:       | 2.42 – 28.68     |                  |
| Theta range      | 3 2 4; 3 2 4     |                  |
| Reference reflections (2) | -13 ≤ h ≤ 11; 0 ≤ k ≤ 11; 0 ≤ l ≤ 17 |                  |
| Measurement area: | 2429             |                  |
| Total reflections | Shelxs and Shexl [14, 15] |                  |
| III – Structure determination | Lorentz and polarization |                  |
| Structure solution | ψ scan [12] |                  |
| Corrections      | 2254             |                  |
| Empirical absorption correction | 164               |                  |
| Reflection with l/σ (l) > 2 | -1.350 and 1.170 e/Å$^3$ |                  |
| Refined parameters | 0.0131           |                  |
| (Δρ)$_{min}$, (Δρ)$_{max}$ (e/Å$^3$) | 0.0252            |                  |
| R$_1$            | 1.021            |                  |
| WR$_2$          |                  |                  |
| S               |                  |                  |

3.1.1. Phosphoric group

The helical (PO$_3$)$_n$ chains in the RbBi(PO$_3$)$_4$ structure, are similar to those of the other alkaline lanthanide polyphosphates [19-21], in which the chains run along the longest unit-cell directions as shown in Figure 2. The polytetraphosphate anion is, as usual in the same group; make up of a chain of eight tetrahedra PO$_4$ sharingorners. The main interatomic distances and bond angles, in the four independent tetrahedra PO$_4$ are given in Table 5. As can be seen, the P – O distances may be divided into linking or bridging P – O(Lij) and exterior P – O(Eij) distances (where O(Lij) denotes the O atom that links P$_i$ with P$_j$ and O(Eij) denotes the j$^{th}$ O atom exterior to the chain and bonded to phosphorus P$_i$) [22]. The linking distances, P – O(Lij), which range from 1.574 to 1.610 Å, are longer than the exterior P – O(Eij) distances, which range from 1.465 to 1.507 Å. The P – O – P angles are understood between 126.2 and 135.4°, which are in good agreement with those usually, met in anions polyphosphates [1-7]. Furthermore, three different types of O – P – O angles co-exist in the PO$_4$ tetrahedra. The O(L) – P – O(L) angles, mean 99.45°, correspond to the longest O – O bonds, the O(L) – P – O(E) and O(E) – P – O(E) angles correspond to the shortest P – O distances, mean 119.22°, probably induced by mutual repulsion of the non-bridging oxygen atoms (Table5). Nevertheless, the calculated mean distortion indices (DI) [23] corresponding to the
different angles and distances in the independent PO₄ tetrahedra [DI (P – O) = 0.0378, DI (O – P – O) = 0.0376 and DI (O...O) = 0.0139] show that the distortion of the P – O distances is greater than that of the O...O distances. The PO₄ tetrahedra therefore have local C₃ symmetry rather than the ideal 43m symmetry [23].

3.1.2. Bismuth coordination

The Bi-atom coordination polyhedra are shown in Figure 4-a, where it can be seen that the irregular eight-coordinate as shows the Bi-O distance. Indeed, these bonds (Bi – O) range between 2.337 and 2.517 Å (Table 5) with a mean distance 2.427 Å, in agreement with the materials belonging to the MBO₃₄ (M = K and Na) family which have been synthesized in our laboratory [10, 11]. The eight-coordinate Bi atom, are exterior oxygen atom (OEij) of the neighboring PO₄ tetrahedra. Although the BiO₆ dodecahedra are considerably distorted, they are isolated from each other in the sense that they do not share any common O atom with the shortest Bi – Bi distance of 5.625 Å. This type of isolation and the coordination number around the Bi-atom is the structural feature that is common to all the polyphosphates. It is to be noted that these dodecahedra BiO₆ are organized in the sense that they formed a zigzag chains according to the [0 1 0] and [0 0 1] directions (Figure 4-b).

3.1.3. Rubidium coordination

While the bismuth is in eight-fold coordination, the rubidium atom is surrounded by ten oxygen atoms (Figure. 5-a). This environment is considerably very irregular as can be seen in other rubidium polytetraphosphates [24-26]. In fact, the Rb – O distances vary from 2.875 to 3.410 Å with an average of 3.153 Å. The RbO₁₀ polyhedra are connected by common corners to (PO₄)₄ chains and by a common edge to bismuth dodecahedra with a Bi-Rb distance of 4.072 Å.

These polyhedra RbO₁₀ are bound tow-by-tow to form chains parallel to the [1 0 1] direction (Figure 5-b). With a comparison of the coordination number around Cs⁺, K⁺, Na⁺ and Li⁺ in the structures CsGd(PO₄)₄ [18], KBi(PO₄)₄ [10], NaBi(PO₄)₄ [11] and LiNd(PO₄)₄ [1] respectively, it can be noted that this number decreases from eleven for CsO₁₁ polyhedra in the first compound to ten for rubidium atom (RbO₁₀) in the title structure, nine for the potassium (KO₃) and six for the octahedra NaO₆ in the second and the third materials, respectively, while only four for LiO₄ tetrahedra in LiNd(PO₄)₄ structure. This result can be explained on the basis of the radii of the monovalent cations that r(Cs⁺) > r(Rb⁺) > r(K⁺) > r(Na⁺) > r(Li⁺), so as the number of oxygen per cation in the chemical formula is constant, it is clear that are passes from an open structure of coordination tetrahedra sharing only some edges in LiNd(PO₄)₄, to a compact framework sharing all edges in CsGd(PO₄)₄, RbBi(PO₄)₄ and KBi(PO₄)₄.

3.2. IR and Raman Spectroscopy Investigations

At room temperature, the compound RbBi(PO₄)₄ exhibits a monoclinic symmetry with space group (P2₁/c, Z = 4). IR and Raman spectra of this compound have been investigated respectively in the frequency range 400 – 1500 and 10 – 1400 cm⁻¹. Figures 6, 7-a and 7-b show IR and Raman spectra of RbBi(PO₄)₄. All the bands were assigned by comparison with the spectra of AgGd(PO₄)₄ [19] and NH₄Ce(PO₄)₄ [27] at room temperature. The frequencies for the corresponding bands are given in table 6.

The infrared absorption spectra of the compound RbBi(PO₄)₄ is characterized by the appearance of only one intense band around 1246 cm⁻¹ which is assigned to the asymmetric vibration νas of (PO₄), this band is observed in the Raman spectra at 1190 cm⁻¹ while the week and strong lines between 1050 and 1150 cm⁻¹ in the IR spectra and between 1030 and 1110 cm⁻¹ in the Raman spectra are attributed to the symmetric vibration νs of (PO₄). The two large bands around 1000 and 930 cm⁻¹ in the IR spectra and some weak and broad peaks around 1000 cm⁻¹ in the Raman spectra are assigned to the asymmetric vibrations νas of (P – O – P). By a comparison with the cyclophosphate KgdP₀₄[26], this band appears after 1030 cm⁻¹. We attribute also, the few bands between 730 and 815 cm⁻¹ in the IR spectra and at 700, 720 and 810 cm⁻¹ in the Raman spectra to the symmetric vibration νs of (P – O – P). All these bands are characteristic of a structure type based on infinite chain of PO₄ tetrahedra bound by a bridge oxygen [21]. We can been note also, that all the bands appears at a frequencies ≤ 200 cm⁻¹ in the Raman spectra are assigned to the translation of the polyphosphate anion (PO₄)₄⁻ and to the translation of the cations (Rb⁺ and Bi³⁺).
Figure 3: The RbBi(PO$_3$)$_4$ structure projected along the a axis

Figure 4 (a): Oxygen environments around the Bi atoms

Figure 4 (b): The BiO$_x$ dodecahedrons projected along the a axis
Figure 5 (a): Oxygen environments around the Rb atoms

Figure 5 (b): The RbO\textsubscript{10} polyhedrons projected along the b axis

Figure 6: IR spectrum of RbBi(PO\textsubscript{3})\textsubscript{4} compound at room temperature
Figure 7: Raman spectrum of RbBi(PO$_3$)$_4$, at room temperature.
(a) in the 10 – 500 cm$^{-1}$ range,
(b) in the 500 – 1400 cm$^{-1}$ range

4. CONCLUSION

In the present work, the single-crystal structure of the rubidium bismuth polyphosphate salts RbBi(PO$_3$)$_4$, synthesized by the flux method, have been reported for the first time. The structure analysis confirms that RbBi(PO$_3$)$_4$ is isostructural with KBi(PO$_3$)$_4$, KGd(PO$_3$)$_4$ and CsGd(PO$_3$)$_4$. It crystallizes in monoclinic system (space group P2$_1$/c), with a structural type IV. The main geometrical feature of this structure is the existence of two infinite (PO$_3$)$_n$ chains, with a period of eight PO$_4$ tetrahedra that is to form two dimensional zigzag sheets along the longest unit-cell directions. In this structure, bismuth atoms are in an eightfold coordination, build infinite dodecahedra organized in the sense that they formed a zigzag chains according to the [0 1 0] and [0 0 1] directions. The coordination polyhedra of the rubidium atoms are made by ten oxygen atoms. The chains (PO$_3$)$_n$ are joined to each other by BiO$_8$ dodecahedra, driving to a three-dimensional framework structure and delimiting tunnels where are lodged Rb$^+$ cations. The structural arrangement around the rubidium cations, can favor the appearance of high ionic conductivity at high temperature and this new type of chain has the largest repeat unit ever observed in the polyphosphate domain, so the polarization measurements and Raman spectroscopy versus the temperature are under way and will give more insight into the mechanism of the structural phase transitions for title compound RbBi(PO$_3$)$_4$.

The infrared and Raman spectra at room temperature of the compound RbBi(PO$_3$)$_4$, are characterized by the apparition of a few bands, confirming the presence of infinite chains of PO$_4$ tetrahedra linked by a bridge oxygen.

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6. ANNEXES

Table 3: Fractional atomic coordinates and temperature factors for RbBi(PO$_3$)$_4$ (Esd given in parentheses)

| Atome | x    | y    | z    | U$_{eq}$ |
|------|------|------|------|---------|
| Bi   | 1.181986(4) | 0.223905(4) | 0.181211(3) | 0.00714(1) |
| Rb   | 0.735911(12) | 0.066780(12) | 0.544890(9) | 0.02383(2) |
| P(1) | 0.69516(3) | -0.10757(3) | 0.01951(2) | 0.00663(4) |
| P(2) | 0.88324(3) | 0.09275(2) | 0.24022(2) | 0.00629(4) |
| P(3) | 0.82121(3) | 0.32504(3) | 0.36156(2) | 0.00602(4) |
| P(4) | 0.52417(3) | 0.47305(3) | 0.273956(19) | 0.00689(4) |
| O(E11) | 0.65519(8) | -0.21241(9) | 0.08499(6) | 0.01536(13) |
| O(E12) | 0.80533(7) | -0.15656(8) | -0.01332(6) | 0.01160(13) |
| O(L12) | 0.75840(8) | 0.04685(8) | 0.09649(6) | 0.01243(14) |
| O(L14) | 0.53866(7) | -0.04569(7) | -0.10617(6) | 0.00946(12) |
| O(E21) | 1.01011(9) | 0.18062(7) | 0.25147(7) | 0.01472(14) |
| O(E22) | 0.92777(8) | -0.03694(8) | 0.32673(6) | 0.01324(13) |
| O(L23) | 0.77336(7) | 0.20486(7) | 0.25361(6) | 0.00962(13) |
| O(E31) | 0.92390(8) | 0.25590(7) | 0.48855(6) | 0.01288(15) |
| O(E32) | 0.86860(8) | 0.46295(7) | 0.32825(7) | 0.01297(13) |
| O(L34) | 0.65293(7) | 0.34334(7) | 0.33883(6) | 0.00838(12) |
| O(E41) | 0.56664(7) | 0.58137(7) | 0.21052(6) | 0.01043(13) |
| O(E42) | 0.36670(7) | 0.40443(8) | 0.19297(6) | 0.01242(14) |

U$_{eq} = \frac{1}{3} \sum \sum U_{ij} a_i^* a_j^* a_i a_j$
Table 4: Anisotropic displacement parameters (in $10^{-3}$ Å$^2$) for RbBi(PO$_3$)$_4$.

| Atome  | $U_{11}$  | $U_{22}$  | $U_{33}$  | $U_{23}$  | $U_{13}$  | $U_{12}$  |
|--------|-----------|-----------|-----------|-----------|-----------|-----------|
| Bi     | 0.01348(1) | 0.00264(1) | 0.00923(1) | -0.00009(1) | 0.00886(1) | 0.00016(1) |
| Rb     | 0.02448(5) | 0.02970(6) | 0.01473(4) | -0.00286(4) | 0.01012(4) | -0.00527(4) |
| P(1)   | 0.01180(11) | 0.00481(10) | 0.00688(10) | -0.00048(7) | 0.00751(9) | 0.00013(8) |
| P(2)   | 0.01385(10) | 0.00666(10) | 0.00904(9) | -0.00126(8) | 0.00934(8) | -0.00075(8) |
| P(3)   | 0.01082(10) | 0.00094(10) | 0.00903(10) | -0.00071(7) | 0.00736(9) | 0.00038(7) |
| P(4)   | 0.01285(12) | 0.00268(10) | 0.00849(12) | -0.00072(8) | 0.00814(10) | -0.00147(8) |
| O(E11) | 0.0270(3) | 0.0083(3) | 0.0188(3) | 0.0054(3) | 0.0179(3) | -0.0017(3) |
| O(E12) | 0.0100(3) | 0.0213(3) | 0.0076(3) | 0.0015(2) | 0.0075(3) | 0.0015(2) |
| O(L12) | 0.0265(3) | 0.0047(3) | 0.0088(3) | -0.0062(2) | 0.0119(3) | -0.0033(2) |
| O(L14) | 0.0132(3) | 0.0070(3) | 0.0145(3) | 0.0014(2) | 0.0117(3) | -0.0022(2) |
| O(E21) | 0.0215(3) | 0.0114(3) | 0.0196(3) | -0.0061(3) | 0.0168(3) | -0.0071(3) |
| O(E22) | 0.0159(3) | 0.0056(3) | 0.0168(3) | 0.0007(2) | 0.0088(3) | -0.0008(2) |
| O(L23) | 0.0169(3) | 0.0028(3) | 0.0117(3) | -0.0058(3) | 0.0099(3) | -0.0014(3) |
| O(E31) | 0.0130(3) | 0.0151(4) | 0.0116(3) | 0.0056(2) | 0.0078(2) | -0.0020(2) |
| O(E32) | 0.0188(3) | 0.0009(3) | 0.0285(3) | 0.0029(3) | 0.0190(3) | 0.0014(2) |
| O(L34) | 0.0132(3) | 0.0000(3) | 0.0151(3) | 0.0023(2) | 0.0101(3) | 0.0010(2) |
| O(E41) | 0.0116(3) | 0.0045(3) | 0.0134(3) | 0.0006(2) | 0.0063(3) | -0.0003(2) |
| O(E42) | 0.0117(3) | 0.0126(4) | 0.0106(3) | -0.0020(3) | 0.0053(3) | -0.0052(3) |

The anisotropic displacement exponent takes the form $\exp \left[-2\pi^2\sum_i \sum_j U_{ij} h_i h_j a_i a_j^* \right]$
Table 5: Bond distances (Å) and angles (°) in RbBi(PO$_3$)$_4$ with standard deviations in parentheses

a. Tetrahedra around P(1)

|       | O(E11)  | O(E12)  | O(L12)  | O(L14)  |
|-------|---------|---------|---------|---------|
| P(1)  | 1.483 (7)| 2.585 (3)| 2.533 (4)| 2.513 (3)|
| O(E11) | 119.6 (4)| 1.507 (6)| 2.535 (3)| 2.501 (3)|
| O(E12) | 110.1 (4)| 109.0 (4)| 1.606 (7)| 2.398 (3)|
| O(L14) | 110.2 (4)| 107.9 (3)| 97.7 (4) | 1.579 (7)|

b. Tetrahedra around P(2)

|       | O(E21)  | O(E22)  | O(L12)  | O(L23)  |
|-------|---------|---------|---------|---------|
| P(2)  | 1.472 (7)| 2.549 (3)| 2.481 (4)| 2.495 (3)|
| O(E21) | 118.8 (4)| 1.489 (7)| 2.527 (3)| 2.532 (4)|
| O(E22) | 109.0 (4)| 111.1 (4)| 1.574 (6)| 2.412 (2)|
| O(L23) | 108.0 (4)| 109.5 (4)| 98.4 (4) | 1.610 (6)|

c. Tetrahedra around P(3)

|       | O(E31)  | O(E32)  | O(L23)  | O(L34)  |
|-------|---------|---------|---------|---------|
| P(3)  | 1.472 (6)| 2.588 (3)| 2.514 (2)| 2.430 (4)|
| O(E31) | 121.9 (4)| 1.489 (7)| 2.483 (3)| 2.569 (3)|
| O(E32) | 109.9 (4)| 107.1 (4)| 1.597 (6)| 2.446 (2)|
| O(L34) | 104.1 (3)| 112.0 (4)| 99.5 (3) | 1.608 (7)|

d. Tetrahedra around P(4)

|       | O(E41)  | O(E42)  | O(L34)  | O(L14)$^iv$ |
|-------|---------|---------|---------|-------------|
| P(4)  | 1.500 (6)| 2.524 (3)| 2.527 (3)| 2.580 (3)|
| O(E41) | 116.6 (4)| 1.465 (7)| 2.477 (3)| 2.471 (2)|
| O(E42) | 109.6 (3)| 108.1 (4)| 1.593 (6)| 2.497 (3)|
| O(L14)$^iv$ | 112.1 (4)| 106.9 (4)| 102.5 (3)| 1.609 (6)|

e. Inter-tetrahedral angle

|       | O(L12) – P(2) | O(L23) – P(3) | O(L34) – P(4) | O(L14) – P(4)$^iv$ |
|-------|----------------|----------------|----------------|---------------------|
| P(1)  | 135.4 (5)      | 130.0 (4)      | 131.4 (4)      | 126.2 (4)           |

a. Polyhedra around Bi

|       | O(E12)$^iv$ | O(E31)$^iv$ | O(E32)$^iv$ | O(E22)$^iv$ |
|-------|-------------|-------------|-------------|-------------|
| Bi    | 2.337 (6)   | 2.365 (6)   | 2.390 (7)   | 2.408 (7)   |
### Polyhedra around Rb

| Bond       | Distance (Å) | Thickness (Å) |
|------------|--------------|---------------|
| Rb – O(E22)$^{	ext{vii}}$ | 2.875 (7)    |               |
| Rb – O(E41)$^{	ext{viii}}$ | 2.937 (7)    |               |
| Rb – O(E42)$^{	ext{viii}}$ | 2.982 (7)    |               |
| Rb – O(E31) | 2.992 (6)    |               |
| Rb – O(E32)$^\text{i}$ | 3.081 (8)    |               |
| Rb – O(L23)$^\text{i}$ | 3.231 (7)    |               |
| Rb – O(E21)$^{	ext{vii}}$ | 3.269 (7)    |               |
| Rb – O(L34) | 3.367 (6)    |               |
| Rb – O(E21)$^\text{i}$ | 3.387 (7)    |               |
| Rb – O(E11)$^\text{IX}$ | 3.410 (8)    |               |

Symmetry code:

I : x, –y + ½, z + ½  
II : x, –y + ½, z – ½  
III : –x + 2, –y, –z  
IV : –x + 2, y + ½, –z + ½  
V : –x + 2, y + ½, –z + ½  
VI : x + 1, y, z  
VII : –x + 2, –y, –z + 1  
VIII : –x + 1, y – ½, –z + ½  
IX : –x, –y – ½, z + ½
Table 6: Raman and Infrared frequencies (cm\(^{-1}\)) and band assignment at room temperature

| IR frequencies (cm\(^{-1}\)) | Raman frequencies (cm\(^{-1}\)) | Assignment |
|-----------------------------|---------------------------------|------------|
| 1246                        | 1249                            | \(\nu_{as}(O-P-O)\) |
| -                           | 1221                            |            |
| -                           | 1190                            |            |
| -                           | 1175                            |            |
| 1143                        | 1107                            | \(\nu_{s}(O-P-O)\) |
| 1086                        | 1063                            | \(\nu_{s}(O-P-O)\) |
| 1068                        | 1037                            | \(\nu_{s}(O-P-O)\) |
| 1000                        | 1000                            | \(\nu_{as}(P-O-P)\) |
| 930                         | -                               |            |
| 812                         | 810                             | \(\nu_{as}(P-O-P)\) |
| 758                         | 720                             | \(\delta(O-P-O)\) |
| 731                         | 700                             |            |
| 689                         | 609                             |            |
| 575                         | 543                             |            |
| 551                         | 527                             |            |
| 510                         | 490                             |            |
| 456                         | 430                             |            |
| 432                         | 420                             |            |
| -                           | 380                             |            |
| -                           | 350                             |            |
| -                           | 317                             |            |
| -                           | 291                             |            |
| -                           | 239                             |            |
| -                           | 196                             |            |
| -                           | 149                             |            |
| -                           | 122                             |            |
| -                           | 73                              |            |
| -                           | 47                              |            |
| -                           | 31                              |            |

\(T(PO_3)^{4-} + T(Rb^+) + T(Bi^{3+})\)