All-dielectric polarization-independent optical angular filter

Qinyu Qian¹,², Changqing Xu¹ & Chinhua Wang¹,²

We report on an all-dielectric, polarization-independent angular filter with one-dimension (1D) photonic crystal (PC) composed of semiconductor compatible Si/SiO₂ pairs. The near-symmetric directional band gap of p- and s-polarized components and Fabry-Pérot (F-P) resonances are utilized to realize efficient polarization-independent angular filtering for normal incidence. The proposed angular filter is designed and experimentally demonstrated in a large area (5 cm × 5 cm) with multilayer sputtering depositions. Experimental measurements show that a divergence angle of the polarization-independently transmitted beam through the angular filtering sample at 1550 nm is 2.2° only and the transmission is as high as 0.8 at normal incidence. The proposed and demonstrated angular filter suggests an effective way to design and implement semiconductor compatible, all-dielectric and polarization-independent angular filters in a fashion of simple structure and easy-fabrication, which is expected to have great applications in lighting, beam manipulation, optical coupling and optical communications.

Full control of light has always been an important subject in optics. An electromagnetic wave can be characterized by its phase, amplitude, frequency, polarization, and propagating direction. Tremendous work has been done to manipulate amplitude¹–³, phase¹–⁴, frequency⁵–⁷ and polarization⁸–¹³. Direction filter (or angular filter) has also been widely studied and is still an important topic today. Zero-index-materials (ZIMs) have been explored for the angular filtering. Ideal ZIMs can filter all non-perpendicular incident waves due to vector matching between ZIMs and surrounding materials. Epsilon-near-zero materials (ENZs) have a permittivity near zero, resulting in a low transmission (0.12 only) due to inherently impedance mismatch and plasmonic metal loss¹². It is also noted that ENZs can work only for one of either p- or s-polarized incident waves exhibit significant difference under off-normal incidences. Photonic crystals (PCs) with Dirac-like conical dispersions (DLCDs) can also be used as an angular filter for specific polarizations¹³–¹⁷, in which PCs with DLCDs can be approximated as a double zero medium (DZM), i.e., permittivity and permeability approach zero simultaneously at the frequency of Dirac-like point. In 2013, Moitra et al. reported a DZM that consists of rods of 10 alternating Si/SiO₂ layers. The DZM shows good angular filtering with high transmission within an angle of 30°¹⁴. However, the DZM also works only for TM polarization, and the fabrication of multilayer Si/SiO₂ rods with a high aspect ratio of 3 μm/0.26 μm (height/width) is difficult, especially in large area. In 2014, Shen et al. proposed a 1D PC with varied periodicity to transmit plane waves of specific incident angle (Brewster's angle) and reflect incident waves of other incident angles¹⁸,¹⁹. However, a specific liquid of certain permeability and permittivity must be used to immerse the device in order to improve its low efficiency. It is also noted that the device can work only at incline incidence at Brewster's angle (as opposed to conventional normal incidence) and, same as other angular filters, works only for p-polarized incidence.

Polarization-independent angular filtering remains still unrealized because of the difficulty in physics in which s- and p-polarized incident waves exhibit significant difference under off-normal incidences. In this work, we proposed and experimentally demonstrated a semiconductor compatible, all-dielectric and polarization-independent 1D PCs to achieve angular filtering for normal incidence. Unlike numerous studies of angular filtering with either ENZs or DZMs (both are of near-zero refractive index and polarization sensitive),

¹College of Physics, Optoelectronics and Energy & Collaborative Innovation Center of Suzhou Nano Science and Technology, Soochow University, Suzhou, 215006, China. ²Key Lab of Advanced Optical Manufacturing Technologies of Jiangsu Province and Key Lab of Modern Optical Technologies of Education Ministry of China, Soochow University, Suzhou, 215006, China. Qinyu Qian and Changqing Xu contributed equally to this work. Correspondence and requests for materials should be addressed to C.W. (email: chinhua.wang@suda.edu.cn)
the proposed polarization-independent angular filter (PIAF) shows no character of near-zero refractive index but employs a near-symmetric band structure of $p$- and $s$-polarized components near the band edge to realize angular filtering of normal incidence. By engineering the frequency of the band edge, omnidirectional gaps above the light line except the $k_y = 0$ point (i.e., the normal incident angle, the only angle at which the incident light can propagate) can be obtained, and high transmission of the filtered light is ensured by the optimization of F-P resonance in the 1D structure. Experimental results demonstrate the polarization-independent and efficient filtering behavior, in which the transmission is as high as 0.80 and the divergence angle of the transmitted beam is only 2.2° at the designed wavelength of 1550 nm.

Results

Figure 1(a) shows a 1D PIAF working at the wavelength of 1550 nm. The unit cell is constructed by alternative silicon (Si) and silicon dioxide (SiO$_2$) layers with thicknesses of $L_1 = 80 \pm 8$ nm and $L_2 = 454 \pm 32$ nm, respectively. The electromagnetic wave is incident from the substrate (SiO$_2$) as shown in Fig. 1(a). Si and SiO$_2$ coatings were alternatively deposited on SiO$_2$ substrate of 5 cm $\times$ 5 cm by ion sputtering. Figure 1(b) shows the SEM photograph of the fabricated 1D all-dielectric PIAF. A near-infrared laser (Agilent Technologies, 81960 A, wavelength tunable from 1503 nm to 1632 nm) and a detector (Thorlabs, PAX5710IR1-T) are used to detect the transmission (Fig. 1(c)). A polarizer and a half waveplate are used to tune the orientation of polarization. The transmission of the incident beam at the designed wavelength of 1550 nm is measured when the PIAF is tilted at different angles as shown in Fig. 1(c). Figure 1(d) shows the angular filtering performance of our fabricated PIAF in that the transmission is 0.8 at normal incidence but falls rapidly to 0.17 and zero when incident angle increases to 2° and 5°, respectively. It is also seen that our fabricated PIAF shows the same angular filtering performance for $p$- and $s$-polarized incidences, which clearly indicates the polarization independent behavior.

To further demonstrate the angular filtering effect, divergence behavior of a diffused laser beam transmitting through the PIAF was measured using the experimental setup shown in Fig. 2(a). The laser beam is firstly expanded by a microscope objective (20 $\times$ ) and then passes through the PIAF. The transmitted beam spot at different locations from the PIAF is recorded by an infrared camera (XENICS, XEVA-1.7–320, 320 $\times$ 256 pixels). Figure 2(b) shows the photographs of the transmitted beam spot and the corresponding quantitative fitting plots using software MATLAB. Excellent angular filtering can be obtained in terms of the observed beam spots. Quantitative evaluation of beam size of the transmitted light at different locations can be obtained by using three-dimensional fitting of these spots to Gaussian beam profile as follow:
where $I$ is the intensity (grayscale value in the photographs), $x$ and $y$ represent the coordinate of the beam spot in the photography. $A$, $B$, $C$ and $D$ are the fitting parameters, in which $A$ is the largest grayscale value in the paragraph, $B$ and $D$ are the $x$-coordinate of the columns and the $y$-coordinate of the rows where the sum of the grayscale value of each pixel is largest, respectively. Figure 2(b–g) are the fitted Gaussian profiles of the experimental beam spots from 20 mm to 41 mm away from the PIAF with a step of 1 mm (only six of them are shown). The fitted beam size $r$ (defined as the distance between the center of spot where the intensity is the largest and the position where the intensity falls to $1/e^2$ of that in the center, $r = \sqrt{2}C$) at different locations are given in Fig. 2(h). The slope of the line in Fig. 2(h) represents the divergence angle of the transmitted beam. Linear fitting from Fig. 2(h) can be performed and the following relations can be obtained: $r = 0.0379d + 5.6240$ where $d$ is the distance from the PIAF to the CCD camera (shown in Fig. 2(a)). The divergence angle of the transmitted beam can be calculated as $\theta = \arctan 0.0379 \approx 2.2^\circ$, which is well consistent with the previous results (Fig. 1(d)).

**Theory**

Theoretical design and analysis can be performed based on the unit cell of the proposed PIAF formed by dielectric layers of high and low refractive index whose thicknesses are, respectively, $L_1 = ma$ and $L_2 = na$, where $a$ is the lattice constant and $m + n = 1$. The generalized design process is as follows: Firstly, two dielectric materials of high and low refractive index and optically lossless at the working wavelength are selected. At designated working wavelength of 1550 nm in our case, Si and SiO$_2$ (the refractive index of Si and SiO$_2$ is 3.48 and 1.44, respectively) are chosen. Then $L_1$ and $a$ with $L_2 = a - L_1$ are adjusted to tune the position of the band edge from which the working wavelength can be mainly determined. It is noted that when either $L_2$ (accordingly $L_1 = a - L_2$, fixed $a$) or the layers of the unit cell can affect the wavelength position of the transmission peak. In our proposed PIAF, the optimized parameters are $L_1 = 0.15a$ and $L_2 = 0.85a$, respectively, with $a = 534$ nm. The incident electromagnetic wave with a wave vector $\mathbf{k} = k_x \mathbf{i} + k_y \mathbf{j}$ can be either $p$- or $s$-polarized waves. For the $s$-polarized wave, the electric field is perpendicular to the $x$-$y$ plane, as is the magnetic field for the $p$-polarized wave (inset in Fig. 3(a)). The projected band structure of $p$- and $s$-polarized waves are shown in Fig. 3(a). The green and blue areas indicate the propagating states of $p$- and $s$-polarized wave incidence, respectively. The white areas represent regions of the directional band gap. Those states in the band gap can propagate in the homogeneous medium but will decay in the PIAF. The red line represents the light line. Above the light line, incident waves from substrate can freely propagate in the PIAF. Below the light line, there exist evanescent modes that cannot reach the PIAF from a faraway source. It is noted that in the first band gap there exist an omnidirectional reflection region, which is defined between the normal incidence band edge and light line\textsuperscript{20}. Above but near (i.e., black line in Fig. 3(a), corresponding to wavelength 1550 nm) the band edge frequency (i.e., $\omega = 0.33 (2\pi c/a)$, wavelength 1618 nm,
horizontal dashed line in Fig. 3(a)), the eigenstate in the PIAF distributes near $k_y = 0$, which indicates that the near-normally incident waves can pass through the PIAF sample. For $k_y \neq 0$, the transmittance will decrease quickly due to the existence of directional band gap. Therefore, such a 1D PC structure can be applied to achieve angular filtering, i.e., only the normal incident waves can transmit through the PC structure, while all other incident waves will be reflected due to the existence of directional band gap. It is also noted that the band diagram of $p$- and $s$-polarized wave above the light line in Fig. 3(a) shows excellent symmetric behavior, which provides solid physical evidence for the polarization independent angular filtering of the proposed PIAF. The angular filtering effect through the PIAF can also be visually observed from the numerical simulation shown in Fig. 3(b). In Fig. 3(b), a point source is placed right under the PIAF. It is seen that the PIAF structure filters effectively the wave components with large $k_y$, while the near-normally incident electromagnetic waves can pass through the PIAF with a small divergence angle. In contrast, when the PIAF is replaced by a pure bulk SiO$_2$ (Fig. 3(c)), it is seen that the transmitted waves of the point source propagate along all directions (spherical waves), as expected, with a wave transform across the interface from SiO$_2$ to air for all of wave components. It should be noted that in Fig. 3(b) and (c), the fields under the PIAF and the reference SiO$_2$ are the total fields resulting from the superposition of incident and reflected light, the fields above the PIAF and the reference SiO$_2$ are the pure transmitted light. It is thus seen that the fields in the "incident space" (lower part of the Figure) is much stronger than those in the "transmission space" (upper part of the Figure). The transmission under "normal incidence" through the PIAF is, in fact, very high, ~0.92 at wavelength 1550 nm in simulation.

The transmission under normal incidence through the PIAF, however, is usually very low due to the mismatched impedance of the 1D PC structure and background media. To increase the energy efficiency, F-P effect

---

**Figure 3.** Theoretical design and analysis of the proposed PIAF. (a) The projected band structure of $p$- and $s$-polarized waves. The red lines represent the light line. The black horizontal line represents the wavelength of 1550 nm, the dashed horizontal line represents the band edge frequency ($\omega = 0.33 (2\pi/c)$, i.e., wavelength of 1618 nm) at $k_y = 0$. (b) Field distribution when a point source is placed under the PIAF; and (c) Field distribution when a point source is placed under a SiO$_2$ bulk as a comparison. The external medium is set as air and the wavelength is 1550 nm.
can be utilized for realizing high transmission and sharp resonant peaks in the transmission spectra. The F-P resonant peaks can be engineered by utilizing the scaling properties of Maxwell’s equations. If the linear dimensions of the structures in a given PC are scaled uniformly by a factor of \( \alpha \), the frequency \( \omega \) and wave vector \( k \) should also be scaled according to the relations \( \omega' = \omega/\alpha \) and \( k' = k/\alpha \). The transmission spectrum for the PIAF structure with different layers of unit cell (8–12 layers) are plotted in Fig. 4(a). The transmission is simulated using the finite difference time domain method (Lumerical FDTD Solutions, Canada). In the simulation, \( L_1 = 80 \text{ nm} \) and \( L_2 = 454 \text{ nm} \) are used. It is seen from Fig. 4(a) that the F-P peaks redshifts and the bandwidth decreases as the layers of Si/SiO\(_2\) pairs increase. Only the rightmost peak can be employed in designing the angular filter because it is the nearest to the band edge. This behavior can be used to tune the working wavelength, as seen in Fig. 4(a) that working wavelength at 1550 nm (black vertical line) can be obtained with a 10-layer PIAF structure with \( L_1 = 80 \text{ nm} \) and \( L_2 = 454 \text{ nm} \). The rightmost peak can be tuned in the range from 1535 nm to 1558 nm (indicated with the peaks in dotted circle in Fig. 4(a)).

The F-P resonant peaks can also be tuned in a wider range by changing the thickness of Si and SiO\(_2\) (\( L_1 \) and \( L_2 \)) in unit cell (Fig. 4(b)) because the band edge is changed when changing \( L_1 \) and \( L_2 \) (in contrast, the band edge is unchanged when changing the number of layers), in which the changing of \( L_1 \) and \( L_2 \) (with fixed \( a = L_1 + L_2 = 534 \text{ nm} \)) will result in the change of permittivity distribution. When the permittivity distribution in the unit has a small perturbation from \( \varepsilon(r) \) to \( \varepsilon'(r) \), the eigenfrequency will be shifted from \( \omega_{\text{th}} \) to \( \omega_{\text{th}}' \) according to the formula:

\[
\left( \frac{\omega_{\text{th}}'}{\omega_{\text{th}}} \right)^2 - 1 \approx \frac{\int [\varepsilon(r) - \varepsilon'(r)] |E_{\text{th}}(r)|^2 dr}{\int \varepsilon(r) |E_{\text{th}}(r)|^2 dr} \tag{2}
\]

where \( E_{\text{th}}(r) \) denotes the field distribution of unperturbed modes. By the guidance of Eq. (2), we can adjust the thickness of silicon (while the total thickness of silicon and silica is fixed) to tune the eigenfrequency (working wavelength). Figure 4(b) demonstrates the tuning capability of transmission peaks for normal incident waves near 1550 nm with a 10-layer PIAF structure. When the thickness of silicon (\( L_1 \)) layer changes from 60 nm to 100 nm, the wavelength of the peak nearest to the band edge can be tuned from 1530 nm to 1575 nm (indicated in the dotted circle in Fig. 4(b)), and the peak at wavelength of 1550 nm can be obtained with \( L_1 = 80 \text{ nm} \) (vertical line in Fig. 4(b)). It is seen from Fig. 4(b) that the F-P peaks redshifts and the bandwidth decreases as \( L_1 \) increases (\( L_2 \) decreases). It should be noted that different combinations of thickness of Si and SiO\(_2\) and also the number of unit cell can be used to obtain a similar performance of the PIAF. The transmission peaks and the corresponding wavelength positions in Fig. 4 can also be calculated and understood based on multi-layer thin film system by transfer matrix method. The detailed calculation and discussion is given in Supplementary Information.

The detailed comparison of the performance between the fabricated PIAF (\( L_1 = 80 \pm 8 \text{ nm} \) and \( L_2 = 454 \pm 32 \text{ nm} \)) and the theoretical (\( L_1 = 80 \text{ nm} \) and \( L_2 = 454 \text{ nm} \)) results are given in Fig. 5. Figure 5(a) and (b) show the comparison of experimental and simulated transmission at normal incidence and at different incident angles from 0° to 30° at wavelength 1550 nm, respectively. It is seen that the experimental results agree well with theoretical simulation. The small deviations in transmission peak and bandwidth in Fig. 5(a) and divergent angle in Fig. 5(b) between the experiment and theory can be mainly attributed to fabrication errors of the device, in which the thickness of each Si/SiO\(_2\) layer may deviate from the designed values (the deviation is typically ~5% from the designed value). To verify the effect of the thickness of each layer on the performance of the transmission (i.e., peak transmission, peak wavelength and bandwidth in Fig. 5(a)), detailed simulations have been performed when the thickness of each layer randomly deviates from the designed value. The simulation results confirm that all the peak transmission, peak wavelength and the bandwidth change when the thickness of each layer deviates from the designed value. The deviation of the thickness of each layer also changes the position of...
the band edge. It can be seen from Fig. 3(a) that the divergent angle decreases when the band edge moves up, leading to a smaller divergent angle in the experiment than that in the simulation, as witnessed in Fig. 5(b). The transmission spectrum under p- and s-polarized incidences almost coincides, which excellently demonstrates polarization-independent angular filtering of the fabricated PIAF.

Discussion
In conclusion, we proposed and experimentally demonstrated an all dielectric angular filter working for incident waves of arbitrary polarization for the first time. An omnidirectional reflection region between the band edge and light line is utilized to reflect off-normally incident waves and transmit near-normally incident waves, and optimized F-P resonance is employed to realize high transmission. The filtering angle at a desired wavelength can be tunable with specified design in accordance with practical requirement. The proposed semiconductor-compatible all dielectric PIAF is easy to fabricate in large area and the working wavelength can be tuned easily by optimizing the number of layers or the fraction of Si and SiO$_2$. The working principle of the proposed PIAF can be easily applied in other wavelength bands by replacing the materials with optimized parameters, which provides a generalized and easy way to implement polarization independent angular filters. The demonstrated PIAF is expected to have great applications in lighting, optical coupling and optical communications where directional beam is required with compact and integrated angular filters, and also in beam shaping and filtering in which noise of high spatial frequency, such as scattered light spots or interfering fringes/patterns resulted from diffractive-beam is required with compact and integrated angular filters, and also in beam shaping and filtering in which noise of high spatial frequency, such as scattered light spots or interfering fringes/patterns resulted from diffraction effects, nonlinear effects and defects in optical material and devices, can be effectively eliminated with the proposed angular filter.

References
1. Liu, L. et al. Broadband metasurfaces with simultaneous control of phase and amplitude. Adv. Mater. 26, 5031–5036 (2014).
2. Arbab, A., Horte, Y., Bagheri, M. & Faraon, A. Dielectric metasurfaces for complete control of phase and polarization with subwavelength spatial resolution and high transmission. Nat. Nanotech. 10, 937–945 (2015).
3. Yu, N. et al. Flat optics: controlling wavefronts with optical antenna metasurfaces. IEEE J. Sel. Top. Quant. 19, 4700423 (2013).
4. Almeida, E., Shalem, G. & Prior, Y. Subwavelength nonlinear phase control and anomalous phase matching in plasmic metasurfaces. Nat. Commun. 7, 10367 (2016).
5. Johnson, S. G. & Joannopoulos, J. D. Three-dimensionally periodic dielectric layered structure with omnidirectional photonic band gap. Appl. Phys. Lett. 77, 3490–3492 (2000).
6. Fink, Y. et al. A dielectric omnidirectional reflector. Science 282, 1679–1682 (1998).
7. Bao, Q. et al. Broadband graphene polarizer. Nat. Photonics 5, 411–415 (2011).
8. Tamada, H., Donumuki, T., Yamaguchi, T. & Matsumoto, S. Al wire-grid polarizer using the s-polarization resonance effect at the 0.8-μm wavelength band. Opt. Lett. 22, 419–421 (1997).
9. Bowers, R. S. et al. Optical characterization of epsilon-near-zero, epsilon-near-pole, and hyperbolic response in nanowire metamaterials. J. Opt. Soc. Am. B 10, 2074–2080 (2015).
10. Pollard, R. J. et al. Optical nonlocalities and additional waves in epsilon-near-zero metamaterials. Phys. Rev. Lett. 102, 127405 (2009).
11. Subramania, G., Fischer, A. J. & Luk, T. S. Optical properties of metal-dielectric based epsilon near zero metamaterials. Appl. Phys. Lett. 101, 241107 (2012).
12. Alekseyev, L. V. et al. Uniaxial epsilon-near-zero and metamaterial for angular filtering and polarization control. Appl. Phys. Lett. 97, 131107 (2010).
13. Huang, X., Lai, Y., Hang, Z. H., Zheng, H. & Chan, C. T. Dirac cones induced by accidental degeneracy in photonic crystals and zero-refractive-index materials. Nat. Mater. 10, 582–586 (2011).
14. Mottina, P. et al. Realization of an all-dielectric zero-index optical metamaterial. Nat. Photonics 7, 791–795 (2013).
15. Xu, C. & Lai, Y. Configurable Dirac-like conical dispersions in complex photonic crystals. Phys. Rev. B 95, 045124 (2017).
16. Xu, C. et al. Angular selection of incident waves by photonic crystals with position-varying Dirac points at the Brillouin zone boundary. Phys. Rev. B 93, 245116 (2016).
17. Wu, Y., Li, J., Zhang, Z. Q. & Chan, C. T. Effective medium theory for magnetodielectric composites: Beyond the long-wavelength limit. Phys. Rev. B 74, 085111 (2006).
18. Shen, Y. et al. Optical broadband angular selectivity. Science 343, 1499–1501 (2014).
19. Shen, Y., Hsu, C. W., Yeng, Y. X., Ioannopoulos, J. D. & Soljačić, M. Broadband angular selectivity of light at the nanoscale: Progress, applications, and outlook. Appl. Phys. Rev. 3, 011103 (2016).
20. Joannopoulos, J. D., Johnson, S. G., Winn, J. N. & Meade, R. D. in Photonic Crystals: Molding the Flow of Light (Princeton University Press, Princeton, 2008).
21. Fang, A., Zhang, Z. Q., Louie, S. G. & Chan, C. T. Klein tunneling and supercollimation of pseudospin-1 electromagnetic waves. Phys. Rev. B 93, 035422 (2016).
22. Zhang, X. et al. Enlarging a photonic band gap by using insertion. Phys. Rev. B 61, 1892 (2000).
23. Lai, Y., Zhang, X. D. & Zhang, Z. Q. Engineering acoustic band gaps. Appl. Phys. Lett. 79, 3224–3226 (2001).

Acknowledgements
The project is supported by National Natural Science Foundation of China (No. 61378057). The work was supported by the project of the Priority Academic Program Development (PAPD) of Jiangsu Higher Education Institutions. The help from Chen Cao during the preparation of the manuscript was acknowledged.

Author Contributions
Q.Y. performed the experiment and numerical simulations. C.X. performed the theoretical analysis. C.W. supervised the project. Q.Y., C.X. and C.W. prepared the manuscript.

Additional Information
Supplementary information accompanies this paper at https://doi.org/10.1038/s41598-017-16837-w.

Competing Interests: The authors declare that they have no competing interests.

Publisher's note: Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made. The images or other third party material in this article are included in the article’s Creative Commons license, unless indicated otherwise in a credit line to the material. If material is not included in the article’s Creative Commons license and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this license, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2017