We study the chiral crossover, the spectra of light-light and of static-light mesons and the deconfinement crossover at finite temperature $T$. Our framework is the confining and chiral invariant quark model, related to truncated Coulomb gauge QCD. Since we are dealing with light quarks, where the linear potential dominates the quark condensate and the spectrum, we only specialize in the linear confining potential for the quark-antiquark interaction. We utilize $T$ dependent string tensions previously fitted from lattice QCD data, and a fit of previously computed dynamically generated constituent quark masses. We scan the $T$ effects on the constituent quark mass, on the meson spectra and on the polyakov loop.
Our main motivation is to contribute to understand the QCD phase diagram \([1]\), for finite \(T\) and \(\mu\). The QCD phase diagram is scheduled to be studied at LHC, RHIC and FAIR, and is sketched in Fig 1. Notice that, after enormous theoretical efforts, the analytic crossover nature of the finite-temperature QCD transition was finally determined by Y. Aoki \textit{et al.} \([2]\), utilizing Lattice QCD and physical quark, and reaching the continuum extrapolation with a finite volume analysis.

Here we utilize the Coulomb gauge hamiltonian formalism of QCD, presently the only continuum model of QCD able to microscopically include both a quark-antiquark confining potential and a vacuum condensate of quark-antiquark pairs. This model is able to address excited hadrons as in Fig. 2, and chiral symmetry at the same token, and we recently suggested that the infrared enhancement of the quark mass can be observed in the excited baryon spectrum at CBELSA and at JLAB \([3, 4]\). Thus the present work, not only addresses the QCD phase diagram, but it also constitutes the first step to allow us in the future to extend the computation of any hadron spectrum, say the Fig. 2 computed in reference \([3]\), to finite \(T\).

Both for the study of the hadron spectra, and for the study the QCD phase diagram, a finite quark mass is relevant. In the phase diagram, a finite current quark mass \(m_0\) affects the position of the critical point between the crossover at low chemical potential \(\mu\) and the phase transition at higher \(\mu\). Moreover the current quark mass affects the QCD vacuum energy density \(\mathcal{E}\), relevant for the dark energy of cosmology. This all occurs in the dynamical generation of the quark mass.
quark mass and meson spectrum at deconfinement

Pedro Bicudo

Figure 2: First calculation of excited baryons with a chiral invariant quark model [3].

$m(p)$. While the quark condensate $\langle \bar{\psi} \psi \rangle$ is a frequently used order parameter for chiral symmetry breaking, the mass gap, i.e. the quark mass at vanishing momentum $m(0)$ is another possible order parameter for chiral symmetry breaking.

Here we address the finite temperature string tension, the quark mass gap for a finite current quark mass and temperature, and the deconfinement and chiral restoration crossovers. We conclude on the separation of the critical point for chiral symmetry restoration from the critical point for deconfinement.

2. Fits for the finite T string tension from the Lattice QCD energy $F_1$

At vanishing temperature $T = 0$, the confinement, due to the formation of chromo-electric and chromo-magnetic flux tubes as shown in Figs. 3 and 4, can be modelled by a string tension, dominant at moderate distances,

$$V(r) \simeq \frac{\pi}{12r} + V_0 + \sigma r.$$  \hspace{1cm} (2.1)

At short distances we have the Luscher or Nambu-Gotto Coulomb potential due to the string vibration plus the One Gluon Exchange Coulomb potential, however the Coulomb potential is not important for chiral symmetry breaking. At finite temperature the string tension $\sigma(T)$ should also dominate chiral symmetry breaking, and thus one of our crucial steps here is the fit of the string ten-
Figure 3: The fields generated by static hybrid sources, notice how the flux organizes into fundamental colour triplet flux tubes.

The fields generated by static hybrid sources, notice how the flux organizes into fundamental colour triplet flux tubes.

σ(\(T\)) obtained from the Lattice QCD data for the quark-antiquark free energy of the Bielefeld Lattice QCD group, [5, 6, 7, 8, 9].

At finite temperature, the quark, or the quark-antiquark free energies, can be computed utilizing Polyakov loops, as in Fig. 5. The Polyakov loop is a gluonic path, closed in the imaginary time \(t_4\) (proportional to the inverse temperature \(T^{-1}\)) direction in a periodic boundary Euclidian Lattice discretization of QCD. They measures the free energy \(F\) of one or more static quarks,

\[
P(0) = Ne^{-F_q/T}, \quad P^\alpha(0)\tilde{P}^\alpha(r) = Ne^{-F_{q\bar{q}}(r)/T}.
\] (2.2)

If we consider a single solitary quark in the universe, in the confining phase, his string will travel as far as needed to connect the quark to an antiquark, resulting in an infinite energy \(F\). Thus the 1 quark Polyakov loop \(P\) is a frequently used order parameter for deconfinement. With the string tension \(\sigma(T)\) extracted from the \(q\bar{q}\) pair of Polyakov loops we can also estimate the 1 quark Polyakov loop \(P(0)\).

At finite \(T\), we use as thermodynamic potentials the free energy \(F_1\) , computed in Lattice QCD with the Polyakov loops [5, 6, 7, 8, 9], and illustrated in Fig. 6. It is related to the static potential \(V(r) = -fdr\) with \(F_1(r) = -fdr - SdT\) adequate for isothermic transformations. In Fig. 7 we
extract the string tensions $\sigma(T)$ from the free energy $F_1(T)$ computed by the Bielefeld group, and we also include string tensions previously computed by the Bielefeld group [10].

We also find an ansatz for the string tension curve, among the order parameter curves of other physical systems related to confinement, i.e., in ferromagnetic materials, in the Ising model, in superconductors either in the BCS model or in the Ginzburg-Landau model, or in string models, to suggest ansatze for the string tension curve. We find that the order parameter curve that best fits our string tension curve is the spontaneous magnetization of a ferromagnet [11], solution of the algebraic equation,

$$\frac{M}{M_{sat}} = \tanh \left( \frac{T_c}{T} \frac{M}{M_{sat}} \right). \quad (2.3)$$

In Fig. 8 we show the solution of Eq. 2.3 obtained with the fixed point expansion, and compare it with the string tensions computed from lattice QCD data.

3. The mass gap equation with finite $T$ and finite current quark mass $m_0$.

Now, the critical point occurs when the phase transition changes to a crossover, and the crossover in QCD is produced by the finite current quark mass $m_0$, since it affects the order parameters $P$ or $\sigma$, and the mass gap $m(0)$ or the quark condensate $\langle \bar{q}q \rangle$. Moreover utilizing as order parameter the mass gap, i.e., the quark mass at vanishing moment, a finite quark mass transforms the chiral symmetry breaking from a phase transition into a crossover. For the study of the QCD
Figure 5: The renormalized Polyakov loop of a single quark, computed by our Lattice QCD group.

phase diagram it thus is relevant to determine how the current quark mass affects chiral symmetry breaking, in particular we study in detail the effect of the finite current quark mass on chiral symmetry breaking, in the framework of truncated Coulomb gauge QCD with a linear confining quark-antiquark potential.

The most fundamental information for the quark-antiquark interaction in QCD comes from the Wilson loop in Lattice QCD, providing the confining quark-antiquark potential for a static quark-antiquark pair. This potential is consistent with the funnel potential, also utilized in the quark model to describe the quark-antiquark sector of meson spectrum, in particular to describe the linear behaviour of mesonic Regge trajectories. Notice that the short range Coulomb potential could also be included in the interaction, but here we ignore it since it only affects the quark mass through ultraviolet renormalization \[12\], which is assumed to be already included in the current quark mass. Here we specialize in computing different aspects of chiral symmetry breaking with linear confinement \( V = \sigma r \). Since we are interested in working at finite temperature \( T \) we utilize a recent fit of lattice QCQ data with a temperature dependent string tension \( \sigma(T) \).

To address the light quark sector it is not sufficient to know the static quark-antiquark potential, we also need to know what Dirac vertex to use in the quark-antiquark interaction. This vertex is necessary to study not only the meson spectrum but also the dynamical spontaneous breaking of chiral symmetry. To determine what vertex to use, we review how the quark-antiquark potential can be approximately derived from QCD, in two different gauges. In Coulomb gauge \[13\],

\[
\nabla \cdot A(x,t) = 0
\]

the interaction potential, as derived by Szczepaniak and Swanson \[14, 15\], is a density-density interaction, with Dirac structure \( \gamma^0 \otimes \gamma^0 \). Another approximate path from QCD considers the mod-
Figure 6: We show examples finite temperature static quark-antiquark potentials, in particular the $T < T_c$ and $T > T_c$. Lattice QCD data for the free energy $F_1$, thanks to [5, 6, 7, 8, 9] Olaf Kaczmarek et al. The solid line represents the $T = 0$ static quark-antiquark potential. In this paper we discuss the use of the free energy as a finite temperature quark-antiquark potential.
ified coordinate gauge of Balitsky [16] and in the interaction potential for the quark sector, retains the first cumulant order, of two gluons [17, 18, 19]. This again results in a simple density-density effective $\gamma^0 \otimes \gamma^0$ confining interaction. As in QCD, this only has one scale, say $K_0$, in the interaction, since both the quark condensate and the hadron spectrum turn out to be insensitive to any constant $U$ in the potential. Thus our framework is similar to an expansion of the QCD interaction, truncated to the leading density-density term, where the confining quark-antiquark potential is a linear potential.

While this is not exactly equivalent to QCD, our framework maintains three interesting aspects of non-pertubative QCD, a chiral invariant quark-antiquark interaction, the cancellation of infrared divergences [20, 21, 22, 23, 24, 25], and a quark-antiquark linear potential [26, 27, 28, 14, 29, 30]. Importantly, since our model is well defined and solvable, it can be used as a simpler model than QCD, and yet qualitatively correct, to address different aspects of hadronic physics. In particular here we study how chiral symmetry breaking occurs at finite temperature $T$ and chemical potential $\mu$, in the realistic case of small but finite current quark masses. Thus we apply our framework to the phase diagram of QCD.

Our interaction potential for the quark sector is,

$$V_I = \int d^3x \left[ \bar{\psi}(x) (m_0 - i\vec{\alpha} \cdot \vec{\nabla}) \psi(x) + \frac{1}{2} \int d^3y \right]$$

$$\bar{\psi}(x)^a \gamma^\mu \psi(x) \frac{-3}{16} V(|x-y|) \bar{\psi}(y)^b \gamma^\mu \psi(y)$$

(3.2)

where the density-density interaction includes just the linear confining potential together with an infrared constant, which may be possibly divergent.

The mass gap equation and the energy of a quark are determined from the Schwinger-Dyson equation at one loop order using the Hamiltonian of Eq. (3.2), for a recent derivation with all
Figure 8: (top) The critical curve for $\frac{M}{M_{sat}}$ as a function of $\frac{T}{T_c}$, for $T \simeq T_c$ it behaves like a square root. (bottom) Comparing the magnetization critical curve with the string tension $\frac{\sigma}{\sigma_0}$, fitted from the long distance part of $F_1$, they are quite close.

details see [31]. The interaction in the four momentum of the potential and quark propagator term includes an integral in the energy

$$\int_{-\infty}^{+\infty} \frac{d p^0}{2\pi} \left( \frac{i}{p^0 - E(p) + i\epsilon} \right) = -\frac{1}{2},$$

(3.3)
Figure 9: The linear potential must be regularized for the Fourier Transform, and we show our two different regularizations both leading to $V(r) \to 0$ when $r \to 0$. Two successions of curves are plotted, leading exactly to linear potentials in the limit of a vanishing infrared regulator $\mu \to \infty$. The regularization of the negative curves maintains the potential monotonous, but adds an infrared negative constant to the potential. The regularization of the positive curves maintains $V(0) = 0$ but the potential decreases for large $r$.

which factorizes trivially from the vector $p$ momentum integral. Using spherical coordinates, the angular integrals can be performed analytically and finally only an integral in the modulus of the momentum remains to be computed numerically. We arrive at the mass gap equation in two equivalent forms, of a non-linear integral functional equation,

$$0 = pS(p) - m_0 C(p) - \frac{\sigma}{p^2} \int_0^\infty \frac{dk}{2\pi} \left[ I_A(k, p, \mu) S(k) C(p) - I_B(k, p, \mu) S(p) C(k) \right],$$

(3.4)
Figure 10: We plot the solution of the mass gap equation \( m(0) \) at \( T = 0 \), for different values of the current quark mass \( m_0 \) in the case where the string tension is \( \sigma = 1 \). We also show, with a solid line, the fit with a two-parameter irrational function.

and of a minimum equation of the energy density \( \mathcal{E} \),

\[
\mathcal{E} = \frac{-g}{2\pi} \int_0^\infty \frac{dp}{2\pi} \left[ 2p^3 C(p) + 2p^2 m_0 S(p) + \sigma \times \int_0^\infty \frac{dk}{2\pi} I_A(k,p,\mu) S(k) S(p) + I_B(k,p,\mu) C(p) C(k) \right],
\]

(3.5)

where the functions \( I_B \) and \( I_A \) are angular integrals of the Fourier transform of the potential. In what concerns the one quark energy we get,

\[
E(p) = pC(p) + m_0 S(p) + \frac{\sigma}{p^2} \int_0^\infty \frac{dk}{2\pi} I_A(k,p,\mu) \times S(k) S(p) + I_B(k,p,\mu) C(p) C(k).
\]

(3.6)

In the chiral limit of massless current quarks, the breaking of chiral symmetry is spontaneous. But for a finite current quark mass, some dynamical symmetry breaking continues to add to the explicit breaking caused by the quark mass. The mass gap equation at the ladder/rainbow truncation.
Figure 11: We plot the mass gap \( m(0) \) as a function of \( T \) for the light \( u \) (lightest) and \( d \) (slightly heavier) quarks. We have a crossover, close to a phase transition, since the current masses of the light quarks are much smaller than the dynamically generated constituent quark mass.
Figure 12: Log plot of the mass gap $m_q(0)$ for the six different flavours of quarks as a function of $T$. From bottom to top we show the quarks $u$, $d$, $s$, $c$, $b$ and $t$. The heavier the quark, the weaker the crossover gets.

large current quark masses. The solution $m(p)$ is shown in Fig. 10 for a vanishing momentum $p = 0$.

At finite $T$, one only has to change the string tension to the finite $T$ string tension $\sigma(T)$ of Eq. (2.3), for different quark masses [35], and also to replace an integral in $p^0$ by a discrete sum in Matsubara Frequencies. Both are equivalent to a reduction in the string tension, $\sigma \to \sigma^*$ and thus all we have to do is to solve the mass gap equation in units of $\sigma^*$. The results are depicted in Fig. 10. Thus at vanishing $m_0$ we have a chiral symmetry phase transition, and at finite $m_0$ we have a crossover, that gets weaker and weaker when $m_0$ increases. This is also sketched in Fig. 10.

4. Infrared regularization of the linear confining potential and the Matsubara sum

Notice that in the case of a linear potential, divergent in the infrared, the Fourier transform needs an infrared regulator $\mu$ eventually vanishing. We illustrate two possible infrared regularizations of the linear potential if Fig. 9.

A possible regularization of the linear potential is,

$$V(r) = -\sigma \frac{e^{-\mu r}}{\mu} \simeq -\frac{\sigma}{\mu} + \sigma r,$$

(4.1)
corresponding to a model of confinement where the quark-antiquark system has an infinite binding energy $\frac{\sigma}{\mu}$ at the origin $r = 0$, is monotonous and only vanishes at an arbitrarily large distance. This
potential has a simple three-dimensional Fourier transform,
\[
V(k) = \int_0^\infty dr \frac{4\pi r \sin(kr)}{k} V(r) \\
= \sigma \frac{-8\pi}{(k^2 + \mu^2)^2}
\]
and this is the most common form of the linear potential in momentum space utilized in the literature. Notice that this is infrared divergent due to the \(-1/\mu\) infinite binding energy in the limit where the regulator \(\mu \to 0\).

If we want to avoid the infinite binding energy we should use a different regularization of the linear potential, also vanishing when \(r \to \infty\) but not monotonous since it grows linearly at the origin starting with \(V(0) = 0\),
\[
V(r) = \sigma r e^{-\mu r}
\]
where the Fourier transform,
\[
V(k) = \sigma \frac{-8\pi}{(k^2 + \mu^2)^2} + \sigma \frac{32\pi \mu^2}{(k^2 + \mu^2)^3}
\]
is such that the integrals in \(k\) no longer diverge. For instance,
\[
\int_{-\infty}^{+\infty} k^2 dk V(k) = 0
\]
Figure 14: Sketch the order parameter \( P \) polyakov loop for the quark antiquark-system, as implied by the saturation of the energy of the quark-antiquark system.

since this is proportional to \( V(0) = 0 \). The new term in the potential \( \frac{32\pi^2 m^2}{(k^2 + \mu^2)} \) is equal to \( (2\pi)^3 \delta^3(k)/\mu \) in the limit \( \mu \to 0 \), and this potential is infrared finite. Both the potentials in Eqs. (4.1) and (4.3) are illustrated in Fig. 9.

In the vanishing temperature limit \( T = 0 \) the different regularizations lead to the same physical results since any constant term in a density-density interaction has no effect in the quark running mass \( m(p) \) or in the hadron spectrum [31]. The regularizations only contribute to the potential and the one-quark energy, but it occurs that these contributions exactly cancel in the chiral order parameters, and in the hadron spectrum.

However at \( T \neq 0 \) the two different regularizations may lead to different physical results.

In the \( T = 0 \) mass gap equation or Schwinger Dyson equation, we have the Minkowsk space integral in \( p^0 \) of the quark propagator pole of Eq. (3.3) and this is equivalent to an integral in \( p^4 \) in Euclidian space after a Wick rotation in the Argand space,

\[
\int_{-\infty}^{+\infty} \frac{id p^4}{2\pi} \frac{i}{ip^4 - E(p) + i\epsilon} = -\frac{1}{2}.
\]

real axis the path corresponds to \( z = p^0 \) and in the imaginary axis the path corresponds to \( z = ip^4 \).

Notice that the integral in Eq. (4.6) is only identical to the one in Eq. (3.3) if the one quark energy \( E(p) > 0 \). If \( E(p) < 0 \) the integral of Eq. (4.6) changes sign, and this is consistent with the pole moving from the fourth quadrant to the third quadrant of the Argand plane. While the integral
in Eq. (3.3) is insensitive to this translation of the pole, the Wick rotation leads to a pole correction. For simplicity, we choose to work with positive one quark energies only $E(p) > 0$.

In finite temperature $T$ and density $\rho$, the continuous euclidian space integration of eq. (4.6) is extended to the sum in Matsubara frequencies,

$$\sum_{n = -\infty}^{\infty} i kT \frac{i}{i(2n + 1)\pi kT - |E(p)|}.$$  \(4.7\)

It is clear that in the vanishing temperature and density $kT << E$ limit one gets back the initial Euclidean space integral of eq. (4.6), when the Matsubara sum approaches the continuum integration with $kT \rightarrow \frac{dP^4}{2\pi}$.

Notice that at $T \neq 0$ the results depend on the constant in the potential. Since the Matsubara sum depends on the one quark energy $E(p)$, and a constant shift of the potential added to the linear term, say $V = \sigma(T) r - U_0 U_0 > 0$, affects the energy by a $\frac{1}{2} U_0$, thus weakening the finite $T$ effects scaling like $\frac{kT}{E}$. On the other hand if the shift is small enough to produce at some $p$ a negative energy $E(p) < 0$, at vanishing density $\mu = 0$, then the Matsubara sum could break down.

Thus we study here only one scenario for the constant potential shift $-U_0$, present anyway in the different possible infrared regularizations of the linear potential. Our scenario consists in a maximum energy, with $U_0 \rightarrow \infty$ as in the standard regularization of the linear potential of Eq. (4.1). In that case $E(p) \rightarrow \infty$ and the Matsubara sum is simply constant, producing always the $T = 0$ result of $\frac{-1}{2}$. Our results are shown in Figs. [1] and [2].

We don’t explore this second possible scenario here, leaving it for a future study, consisting in having the minimal $U_0$, closer to the regularization of the linear potential of Eq. (4.3), just sufficient to cancel the one quark energy at vanishing momentum $E(0) = 0$. In that case the Matsubara sum makes a larger difference, interpolating between 0 at vanishing momentum and $-\frac{1}{2}$ at large momentum. But we expect that, whatever the contribution of the Matsubara sum is, the temperature
dependence of the string tension $\sigma(T)$ is the dominant finite $T$ effect, and thus for a first exploration our first scenario is sufficient.

5. Chiral symmetry and confinement crossovers with a finite current quark mass

We now study whether the two main phase transitions in the QCD phase diagram, confinement and chiral symmetry breaking, have two different two critical points or a coincident one. Confinement drives chiral symmetry breaking, and at small density both transitions are a crossover, and not a first or second order phase transition due to the finite quark mass.

However the quark mass affects differently these two phase transitions in the QCD. In what concerns confinement, the linear confining quark-antiquark potential saturates when the string breaks at the threshold for the creation of a quark-antiquark pair. Thus the free energy $F(0)$ of a single static quark is not infinite, it is the energy of the string saturation. The saturation energy is of the order of the mass of a meson i. e. of $2m_0$. For the Polyakov loop we get,

$$P(0) \simeq Ne^{-2m_0/T}. \quad (5.1)$$

Thus at infinite $m_0$ we have a confining phase transition, while at finite $m_0$ we have a crossover, that gets weaker and weaker when $m_0$ decreases. This is sketched in Figs. [3] and [4].

Since the finite current quark mass affects in opposite ways the crossover for confinement and the one for chiral symmetry, we conjecture that at finite $T$ and $\mu$ there are not only one but two critical points (a point where a crossover separates from a phase transition). Since for the light $u$ and $d$ quarks the current mass $m_0$ is small, we expect the crossover for chiral symmetry restoration critical to be closer to the $\mu = 0$ vertical axis, and the crossover for deconfinement to go deeper into the finite $\mu$ region of the critical curve in the QCD phase diagram depicted in Fig. [1].

We now compute the hadron spectrum, in particular the meson spectra. In what concerns the light meson masses $M_{q\bar{q}}$ are dominated by the linear confining potential. At $T_c$, the string tension
\( \sigma(T) \) vanishes, the confining potential disappears, and thus all light hadrons decrease their mass until they melt at \( T = T_c \). Notice that chiral symmetry is not entirely restored because \( m_0/\sqrt{\sigma(T)} \) increases with \( T \). Nevertheless, with \( T \neq 0 \), the masses and wavefunctions do essentially scale with \( \sigma(T) \), and thus also essentially vanish at \( T = T_c \). This is sketched in Fig. 15. A comparable vanishing of light meson masses also occurs in the sigma model [36].

In what concerns the heavy meson masses \( M_{Q\bar{Q}} \), the Coulomb potential is also relevant, and thus the groundstates of the heavy mesons still bind above \( T_c \). Thus while the light mesons melt at \( T = T_c \), the heavy meson groundstates melt at a \( T > T_c \) [37, 38], as depicted in Fig. 16.

6. Outlook

We remark that the pure gauge string tension \( \sigma(T) \) is well fitted by the condensed matter physics magnetization curve \( \chi \), and we utilize it.

We compute the dynamically generated quark mass \( m(p) \), solving the mass gap equation both for finite current quark masses \( m_0 \) and for finite \( T \). The finite current quark masses turn both the confinement and the chiral symmetry phase transitions into two different crossovers.

We qualitatively study the full spectra of light hadrons at finite \( T \), including the excited spectra, and conclude that the light hadron masses essentially vanish at \( T = T_c \). The light hadrons all melt at \( T = T_c \), since the masses and wavefunctions essentially scale with \( \sigma(T) \).

We soon plan to complete the part of this work which is only sketched here, i. e. to compute the excited hadron spectrum at finite \( T \), continuing the work initiated with Tim Van Cauteren, Marco Cardoso, Nuno Cardoso and Felipe Llanes-Estrada [3], and to compute and compare the crossover curves for the chiral symmetry restoration and for the deconfinement at finite \( T \).
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