Born in a Pair (?): Pisces II and Pegasus III*

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Abstract

We have used $B$, $V$ time-series photometry collected with the Large Binocular Telescope to undertake the first study of variable stars in the Milky Way ultra-faint dwarf (UFD) satellites Pisces II and Pegasus III. In Pisces II we have identified an RRab star, one confirmed and a candidate SX Phoenicis star, and a variable with uncertain classification. In Pegasus III we confirmed the variability of two sources: an RRab star and a variable with uncertain classification, similar to the case found in Pisces II. Using the intensity-averaged apparent magnitude of the bona fide RRab star in each galaxy, we estimate distance moduli of $(m-M)_0 = 21.22 \pm 0.14$ mag ($d = 175 \pm 11$ kpc) and $21.21 \pm 0.23$ mag ($d = 174 \pm 18$ kpc) for Pisces II and Pegasus III, respectively. Tests performed to disentangle the actual nature of variables with an uncertain classification led us to conclude that they most likely are bright, long-period, and very metal-poor RRab members of their respective hosts. This may indicate that Pisces II and Pegasus III contain a dominant old stellar population ($t > 12$ Gyr) with metallicity $\langle [\text{Fe/H}] \rangle = -1.8$ dex along with, possibly, a minor, more metal-poor component, as supported by the $V$, $B-V$ color–magnitude diagrams of the two UFDs and their spectroscopically confirmed members. The metallicity spread that we derived from our data sample is $\gtrsim 0.4$ dex in both systems. Lastly, we built isodensity contour maps that do not reveal any irregular shape, thus making the existence of a physical connection between these UFDs unlikely.

\textit{Unified Astronomy Thesaurus concepts:} Dwarf galaxies (416); Galaxy distances (590); Variable stars (1761)

Supporting material: machine-readable table

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1. Introduction

Extensively under investigation in the past couple of decades, the mechanisms leading to the Milky Way (MW) formation and evolution and the role played by the MW dwarf spheroidal (dSph) satellites in assembling the Galaxy we observe today are still a very hot topic of modern astronomy. Under the current $\Lambda$CDM paradigm, these old satellites could be survivors of the accretion events that led to the formation of the stellar halos of the large galaxies they orbit around (Bullock & Johnston 2005; Sales et al. 2007; Stierwalt et al. 2017). Therefore, the MW dSphs are privileged laboratories, contributing to our understanding of the universe on both local and cosmological scales. The MW dSphs are close enough to be resolved in stars, thus allowing us to study the buildup of the MW halo by exploiting information arising from the stars by which they are composed. In the past 20 yr, observations carried out by wide-field surveys like the Sloan Digital Sky Survey (SDSS; York et al. 2000) have increased extraordinarily the numbers of companions detected around the MW. Since 2005, the SDSS has revealed that the MW is surrounded by a new class of satellites, the ultra-faint dwarf (UFD) galaxies. UFDs have low stellar densities that make them very hard to detect unless specific techniques are applied to very large data sets, such as those provided by the SDSS. This survey, along with other imaging surveys such as the Dark Energy Survey (DES; The Dark Energy Survey Collaboration 2005), Pan-STARRS1 3π (Chambers et al. 2016), ATLAS (Shanks et al. 2015), and strategic programs like the Subaru Hyper Suprime-Cam Survey (HSC; Aihara et al. 2018), here has increased the number of new MW satellites (UFDs and stellar clusters) up to 47 (Drlica-Wagner et al. 2015; Laeves et al. 2015; Torrealba et al. 2016; Homma et al. 2019), and references therein). UFDs (see Simon 2019 for a state-of-the-art study on UFDs) are characterized by low surface brightness $\mu_v \geq 28$ mag arcsec$^{-2}$ and luminosities $-8 \leq M_V \leq -1.5$ (Martin et al. 2008), hence resulting in fainter than all previously known dSphs (hereafter, classical dSphs) and the bulk of Galactic globular clusters (GCs). On the absolute visual magnitude versus half-light radius ($M_V-\mu_v$) plane, they populate the extension to lower luminosities of the classical dSphs (see, e.g., Figure 8 in Belokurov et al. 2007; Figure 3 in Clementini 2010). These systems are believed to be strongly dark-matter dominated, as their mass-to-light ratios and velocity dispersions are much higher than for the classical MW satellites (Strigari et al. 2008). Many UFDs present an irregular shape often interpreted as evidence for tidal interaction with the MW (Belokurov et al. 2007; Muñoz et al. 2010); however, their distorted morphologies seem to be more due to lack of deep enough observations rather than the signature of MW tidal stripping (Simon 2019, and references therein). It has been shown that the metal content in the UFDs is lower than in the classical dSphs and very similar to the chemical composition of extremely metal-poor Galactic halo stars and the most metal-poor Galactic GCs (e.g., Kirby et al. 2008), making them likely the direct descendants of the first generation of galaxies in the universe (Bovill & Ricotti 2009; Salvadori & Ferrara 2009). All UFDs, except Leo T (Clementini et al. 2012), have no signature of ongoing star formation activity and display significant spreads in metallicity spanning $[\text{Fe/H}]$ values down to $-4$ dex (see...
Tolstoy et al. (2009, and references therein). They typically host metal-poor ([Fe/H] \leq -2 \text{ dex}) populations older than 10 Gyr as revealed by accurate spectroscopic studies of their stellar content (see, e.g., Simon & Geha 2007; Kirby et al. 2008; Norris et al. 2010; Simon et al. 2011; Kopenov et al. 2015). Consistently with being populated by an old stellar population, and with the only exceptions of Carina III (Torrealba et al. 2018) and Willman I (Siegel et al. 2008), the UFDs that were studied for variability so far have been found to contain at least one RR Lyrae star. RR Lyrae variables (RRLs) are primary distance indicators and tracers of the oldest stellar population in the systems where they reside. RRLs oscillating in the fundamental (RRab) and first-overtone (RRc) pulsation modes occupy two different and well-defined regions in the period–amplitude diagram (Bailey diagram; Bailey 1902; Bailey & Pickering 1913; Bailey et al. 1919). According to the mean period of RRab stars ([P_{ab}]) and the fraction of RRc stars, the RRLs in the MW field and GCs divide into Oosterhoff type I (Oo I) and Oosterhoff type II (Oo II) groups; this phenomenon is known in the literature as Oosterhoff dichotomy (Oosterhoff 1939). The Oo I systems are more metal-rich ([Fe/H] \sim -1.5 \text{ dex}) and their RRLs have shorter periods ([P_{ab}] \sim 0.55 \text{ days}) and a fraction of RRc stars around 17%. The Oo II systems are mostly metal-poor ([Fe/H] \sim -2.0 \text{ dex}), with longer RRab periods ([P_{ab}] \sim 0.65 \text{ day}) bluer horizontal branches (HBs) than the Oo I systems, and a higher fraction of RRc stars (~37%). The properties of the RRLs and the Oosterhoff types observed in the MW halo (dSphs, GCs, and field) can put constraints on the substrutures that contributed in the past to the formation of the MW. The photometric studies carried out to define the pulsation properties of the RRLs in the MW satellites have revealed that the classical dSphs do not generally conform to the Oosterhoff dichotomy and, with the exception of Sagittarius and Ursa Minor, are all classified as Oosterhoff–Intermediate (Mateo 1998). Conversely, the UFDs for which a study of the variable stars has been carried out and RRLs have been identified (21 UFDs so far), although containing only very few such variables (hence, a robust Oosterhoff classification is not possible), mainly tend to host RRLs with Oo II properties, as observed for the variables in the MW GCs and halo (Clementini 2010).

In this paper we present a study of the stellar population and variable star content of the Pisces II (Psc II) and Pegasus III (Peg III) UFDs, based on B, V time-series photometry obtained with the Large Binocular Telescope (LBT). The wide field of view (FOV) of the two cameras of the LBT allowed us to image an area corresponding to about 9 half-light radii in each individual pointing of Psc II and about 12 half-light radii for Peg III. We also investigate the possible physical connection between the two systems from the comparison of their properties (distance, color–magnitude diagrams [CMDs], and variable star populations).

The paper is organized as follows. In Section 2 we present an overview of our targets. In Section 3 we describe the observations and the data reduction. In Sections 4–7 we discuss results from the identification and characterization of the variable stars, discuss the Oosterhoff classification, and measure the distance to Psc II and Peg III using the RRLs. In Section 8 we compare the CMDs of Psc II and Peg III with stellar evolution models. In Section 9 we discuss the capability to retain and lose metals in low-mass galaxies such as our targets, and in Section 10 we present isodensity contour maps. Finally, Section 11 summarizes our results.

### 2. Pisces II and Pegasus III

The Psc II UFD ([RA(J2000) = 22^h 25^m 31^s, decl. (J2000) = 5° 57' 9''; l = 79° 21', b = -47° 11']) was discovered in the southern Galactic portion of the SDSS Segue survey (Yanny et al. 2009) by Belokurov et al. (2010) and later studied in more detail by Sand et al. (2012) and Kirby et al. (2015). Using deep wide-field photometry obtained with Megacam at the Magellan Clay telescope, Sand et al. (2012) estimated the structural and photometric parameters of Psc II. From the mean magnitude of the HB they derived the distance modulus of 21.31 ± 0.17 mag, corresponding to a heliocentric distance of 183 ± 15 kpc. Sand et al. (2012) also estimated a half-light radius of 1.1 ± 0.2 kpc, which delimits the region containing the bulk of the Psc II stars and, at the estimated heliocentric distance, corresponds to a linear extension of 58 ± 10 pc and an absolute magnitude M_V = -4.1 ± 0.4 mag for Psc II. From the comparison of the galaxy CMD with theoretical isochrones by Girardi et al. (2004) and Dotter et al. (2007, 2008), Sand et al. (2012) concluded that Psc II hosts a dominant old (>10 Gyr) and metal-poor ([Fe/H] \sim -2 \text{ dex}) stellar population. Kirby et al. (2015) carried out a spectroscopic study of Psc II using the Keck DEIMOS spectrograph. Their radial velocity measurements confirm the membership of seven candidate RGB stars, leading to a systemic velocity \langle v_c \rangle = -226.5 ± 2.7 \text{ km s}^{-1}. They also measured spectroscopic metallicities for four of the seven confirmed members (see Table 1, upper portion), finding an average value of \langle [Fe/H] \rangle = -2.45 ± 0.07 \text{ dex} and a metallicity dispersion of \sigma_{[Fe/H]} = 0.48 ± 0.70 \text{ dex}. Finally, Kirby et al. (2015) estimated values of \sigma = 5.4^{+3.6}_{-2.4} \text{ km s}^{-1} for the velocity dispersion, log(M/M_\odot) = 6.2^{+0.3}_{-0.2} \text{ for dynamical mass, and } M/L_V = 370^{+310}_{-240} \text{ } M_\odot/L_\odot \text{ for mass-to-light ratio, hence confirming that Psc II is a dark-matter-dominated system.}

A few years later another new MW UFD, Peg III ([RA(J2000) = 22^h 24^m 48^s, decl. (J2000) = 5° 24' 18'', l = 69° 85', b = -41° 83']), was discovered from an analysis of the SDSS Data Release 10 (DR10; Ahn et al. 2014) and then confirmed with deeper Dark Energy Camera (DECam) follow-up observations by Kim et al. (2015). The physical properties derived for Peg III are very similar to those of other previously known MW UFDs, and indeed, Peg III perfectly locates in the UFD region of the MF–\text{r}_h diagram. A further study of this galaxy was carried out by Kim et al. (2016), who, using deeper photometry and spectroscopy data from the Magellan/Baade Telescope Inamori-Magellan Areal Camera & Spectrograph (IMACS), provided a better definition of the Peg III structural and photometric parameters. By fitting the HB fiducial line of the Galactic GC M15 ([Fe/H] = -2.42 dex; Bernard et al. 2014) to the blue horizontal branch stars, Kim et al. (2016) derived a distance modulus (m - M_B = 21.66 ± 0.12 mag corresponding to a heliocentric distance d_L = 215 ± 12 kpc. Using spectroscopic data obtained with the Keck DEIMOS spectrograph, they also measured the radial velocity of a number of candidate members confirming the membership to Peg III of seven of them and obtaining a systemic velocity of -222.5 ± 2.6 km s^{-1}. A further candidate member has a radial velocity about 30 km s^{-1} larger than the systemic velocity inferred from the other seven stars; hence, its actual membership to Peg III remains doubtful. The radial velocities of the eight stars are listed in Table 1 (lower portion). The position of the spectroscopically
Table 1

| ID            | R.A. (J2000) | Decl. (J2000) | \(v_c\) | [Fe/H] |
|---------------|--------------|---------------|---------|--------|
| M1-9004       | 344.57314    | 5.92161       | −224.9 ± 1.6 | −2.38 ± 0.13 |
| M2-9833       | 344.58857    | 5.95573       | −226.9 ± 3.2  | ... |
| M3-10694      | 344.60458    | 5.9572        | −232.0 ± 1.6  | −2.70 ± 0.11 |
| M4-12924      | 344.64224    | 5.96213       | −221.6 ± 2.9  | −2.10 ± 0.18 |
| M5-13387      | 344.64976    | 5.95625       | −215.8 ± 7.6  | ... |
| M6-13560      | 344.65311    | 5.96841       | −223.6 ± 5.3  | −2.15 ± 0.28 |
| M7-14179      | 344.66411    | 5.93354       | −224.8 ± 9.6  | ... |

Pegasi III (Kim et al. 2016)

| ID   | R.A. (J2000) | Decl. (J2000) | \(v_c\) | [Fe/H] |
|------|--------------|---------------|---------|--------|
| M1   | 336.09960    | 5.4118042     | −226.16 ± 5.04 | −2.24 ± 0.15 |
| M2   | 336.11029    | 5.4159619     | −229.45 ± 5.29 | −2.55 ± 0.15 |
| M3   | 336.11378    | 5.4077994     | −218.51 ± 3.64 | −2.55 ± 0.15 |
| M4   | 336.09539    | 5.3958641     | −234.68 ± 3.84 | ... |
| M5   | 336.10025    | 5.424227      | −218.26 ± 3.56 | −2.24 ± 0.15 |
| M6   | 336.10207    | 5.3891321     | −220.57 ± 4.71 | ... |
| M7*  | 336.08666    | 5.39347       | −193.35 ± 22.92 | ... |
| M8   | 336.07518    | 5.4196487     | −208.45 ± 6.66 | ... |

Note.

*Uncertain membership.

confirmed member stars and the comparison of the CMD with the Dartmouth isochrones (Dotter et al. 2008) led Kim et al. (2016) to conclude that Peg III has a dominant old (13.5 Gyr) and metal-poor ([Fe/H] = −2.5 dex) stellar population, in excellent agreement with most of the MW UFD satellites.

The new values of the half-light radius \(r_h = 0.85 ± 0.22\), which at the new heliocentric distance corresponds to \(r_h = 53 ± 14\) pc and absolute magnitude \((M_V = −3.4 ± 0.4\) mag) do not dramatically change the position of Peg III on the \(M_V−r_h\) diagram and keep the galaxy in the UFD region.

Kim et al. (2016) measured the spectroscopic metal abundance of the four brightest stars among the confirmed members, obtaining metallicity estimations from \(−2.24 ± 0.15\) dex to \(−2.55 ± 0.15\) dex. These values are in good agreement with the metallicity inferred from the fit with the old and metal-poor Dartmouth isochrone. The velocity dispersion \(\sigma_v = 5.4 ± 0.2\) km s\(^{-1}\), the dynamical mass \(M_1/2 = 1.4^{+3.0}_{−1.1} \times 10^9\) \(M_\odot\), and the mass-to-light ratio \(M/L_V = 1470^{+5660}_{−1240}\) \(M_\odot/L_\odot\) confirm that Peg III is more dark-matter dominated than Psc II. In addition, Kim et al. (2016) provide a density contour map that shows the irregular shape of the Peg III structure, mostly in the outermost regions. This could be the sign of an ongoing interaction. Finally, Kim et al. (2015, 2016) noticed that Peg III is spatially close to Psc II. They are separated by only 85" on the sky and have fairly similar distances. The spatial separation of the two UFDs is \(\sim 43 ± 19\) kpc (Kim et al. 2016). If Psc II and Peg III do indeed form a physical pair, they could resemble the case of Leo IV and Leo V (de Jong et al. 2010), for which an origin related to a single, tidally disrupted progenitor has been proposed. However, they could also resemble the couple Carina II and Carina III (Torrealba et al. 2018), which have a projected separation of only 18" on sky, hence smaller than Leo IV and Leo V, but are not a pair of bound systems according to Li et al. (2018). The parameters derived in previous studies of Psc II (Belokurov et al. 2010; Sand et al. 2012; Kirby et al. 2016) and Peg III (Kim et al. 2016) are summarized in Table 2.

3. LBT Observations and PSF Photometry of Psc II and Peg III

B, V time-series photometry of Psc II was collected with the Large Binocular Cameras (LBCs; Giallongo et al. 2008) of the LBT program (PI: G. Clementini), which targeted also the MW UFD Peg III. Each LBC has an FOV of 23′ × 23′ and is equipped with four 2048 × 4608 pixel EEV CCDs, resulting in a
6150 × 6650 pixel equivalent detector, with a pixel scale of 0′′.224 pixel −1. The data consist of 26 B and 26 V images for Psc II and 28 B and 28 V images for Peg III, each with an exposure time of 180 s, acquired over six nights from 2015 October to December. This exposure time allowed us to obtain a signal-to-noise ratio of 40 at 21 mag, which roughly corresponds to the minimum in the B and V light curves of RR LFs, according to the Psc II and Peg III distance moduli. Most of the observations were obtained with seeing ≤1′′.2. This is well suited for our purposes. A log of the Psc II and Peg III observations is provided in Table 3. All images were pre-reduced (bias-subtracted, flat-fielded, and astrometrized) by the LBT team through an LBC dedicated pipeline, and then, on each of the four CCDs of the two LBCs, separately, we performed point-spread function (PSF) photometry with the DAOPHOT-ALLSTAR-ALLFRAME packages (Stetson 1987, 1994). To transform the instrumental magnitudes to the Johnson standard system, we used standard stars selected from the SDSS catalog and the transformation equations available at https://www.sdss3.org/dr9/algorithms/sdssUBVRITransform.php#Lupton2005. We used calibration equations of the form \( B − b = c_B + m_B × (b − v) \) and \( V − v = c_V + m_V × (b − v) \), where \( B \) and \( V \) are the standard Johnson magnitudes of the SDSS stars and \( b \) and \( v \) are the instrumental magnitudes in our photometric catalogs. The parameters of the calibration were derived by applying a 3σ clipping rejection algorithm to fit the data. The final fit to calibrate the Psc II catalog was obtained using a total of 772 stars and provided the following calibration equations: \( B − b = 8.229 − 0.1409 × (b − v) \) and \( V − v = 8.195 − 0.0728 × (b − v) \), with the rms values of 0.03 and 0.025 mag for the \( B \) and \( V \) magnitudes, respectively. These calibration equations, derived independently for Psc II and Peg III, are fully consistent with each other. Our final \( B, V \) combined catalogs of sources observed in the LBT fields centered on Psc II and Peg III each contain more than 28,000 objects. The photometric errors for nonvariable sources in our catalogs typically range from 0.0015 up to 0.01 mag for \( B < 20.0 \) mag, from 0.01 up to 0.15 mag for 20.0 mag < \( B < 25 \) mag, and then increase steeply for \( B > 25 \) mag. In particular, the photometric errors at the HB level are about 0.06–0.07 mag in \( V \) and \( B \) for both galaxies. Unfortunately, an unexpected rotation of the LBT occurred during the observations of Peg III. Therefore, some portions of the FOV covered by our observations were deeper than others, causing the detection of fainter sources in those parts of the sky. This produced a more populated CMD but also fictitious overdensities in the density maps, as we further discuss in Section 10.

4. Variable Stars: Identification and Pulsation Properties

To identify variable stars in Psc II and Peg III, we first considered stellar sources with a high value of the variability index computed by DAO MASTER (Stetson 1994) in both the \( B \) and \( V \) passbands. Then, we also checked all stars that in the CMDs of our two targets have colors and magnitudes falling within the edges of the classical instability strip (IS). For Psc II this procedure returned a list of ~20 candidate variables with more than 22/24 data points on the light curves that were visually inspected with the GRaphical Analyzer of Times Series package (GRATIS; Clementini et al. 2000). GRATIS uses the Lomb periodogram (Lomb 1976; Scargle 1982) to obtain a first guess of the star periodicity and then the best fit of the folded light curve with a truncated Fourier series to refine the star period. The final adopted periods were those that minimize the rms scatter of the truncated Fourier series best fitting the data. Taking into account the period, the shape of the light curve, and the position on the CMD according to the intensity-averaged \( B, V \) magnitudes, we confirmed the variability of three candidates and classified in type two of them: one RRab and one SX Phoenicis (SX Phe) star, whereas the classification of the third confirmed variable remains uncertain because two alternative periods are equally probable for the star. Correspondingly, this variable could be either a metal-poor RRab or an anomalous Cepheid (AC). Since the available data did not allow us to firmly establish the correct periodicity, and hence classification in type, of this source, in this work we used both periodicities to fold the star light curves. A forth source, which is located inside the galaxy \( r_p \), exhibits variability particularly in the \( B \) passband. We tentatively classified this source as an SX Phe star; however, this classification remains doubtful because the \( V \) light curve shows very little, if any, variability (see Figure 1). The \( B, V \) time-series photometry of the variable stars identified in Psc II is provided in the upper portion of Table 4. The properties of the variable stars are summarized in the upper portion of Table 5. Column (1) of Table 5 provides the star identifier. This is an increasing number starting from the galaxy center, for which we have adopted the coordinates of the discovery paper (Belokurov et al. 2010). Columns (2) and (3) give the star coordinates. Columns (4), (5), and (6) list, respectively, the classification in type, the period (\( P \)), and the Heliocentric Julian
Day (HJD) of maximum light. Columns (7), (8), (9), and (10) provide the intensity-averaged mean $B$ and $V$ magnitudes and the corresponding amplitudes of the light variation. The $B$, $V$ light curves of the confirmed (three) and candidate (one) variable stars in Psc II are shown in Figure 1. The spatial distribution of all stars measured in our LBT observations of Psc II with respect to galaxy center (R.A., decl.) is shown in Figure 2. In the figure we have marked in blue five ellipses representing from one to five times the $r_h$ of Psc II, 1′.1 ± 0′.2, as estimated by Sand et al. (2012). The bona fide RRab star (V1; magenta filled square) is located within the Psc II $r_h$, at a distance from the center of about 0′.3. The SX Phe star (V3; cyan triangle) and the variable with uncertain type (V4; red filled circle) both are outside the galaxy $r_h$, at distances of about 2′.6 and 4′.5 from the galaxy center. In particular, the SX Phe star is within 3 $r_h$ and the variable with uncertain type within 5 $r_h$. The distance from the galaxy center and the position on the CMD (see Figure 8) of bona fide RRab and SX Phe stars suggest that they belong to Psc II; conversely, the membership of V4 remains doubtful (see Section 7). In Peg III the same procedure as applied for Psc II allowed us to confirm the variability of two sources in our list of candidates: an RRab
star, according to the period, the shape of the light curve, the position on the CMD, and the B, V mean magnitudes; and a variable star with uncertain classification. As for V4 in Psc II, GRATIS finds two equally possible periodicities for the Peg III variable with an uncertain classification. We used both periodicities to fold the star light curves. According to the two different periods, the corresponding amplitudes of the light variation, and the V mean magnitude being about 0.3 mag brighter than the HB level in Peg III, similarly to V4 in Psc II, this variable could be either a very metal-poor RRab or an AC. A few additional B and V measurements would be sufficient to improve the light curve sampling and the period definition, thus allowing us to definitively classify this variable. The B and V time-series photometry and the properties of the two variable stars we have identified in Peg III are provided in the lower portions of Tables 4 and 5, respectively. We have named them V1 and V2 according to their distance from the galaxy center for which we adopted the coordinates by Kim et al. (2016). V1 corresponds to the RRab star, and V2 is the variable of uncertain type. Their B and V light curves are shown in Figure 3, where the data of V2 were folded using the periodicity as RRab in the middle panel and the periodicity as AC in the bottom panel. Figure 4 shows the spatial distribution of all the stars measured in our LBT observations with respect to the center of Peg III. We have marked V1 with a red filled circle, V2 with a red open circle, spectroscopically confirmed members (according to Kim et al. 2016) with blue stars, and an ambiguous member with an orange star. In the figure, five green ellipses indicate, in increasing order, 1, 2, 3, 5, and 10 times the half-light radius ($r_{hl}$) of Peg III, $r_{hl} = 0.85 \pm 0.22$ as computed by Kim et al. (2016). The two confirmed variable stars lie outside the galaxy’s $r_{hl}$ at distances from the galaxy center of 2.5 for the bona fide RRab and 5/8 for the uncertain type variable. The bona fide RRab is within 4 $r_{hl}$, and its position on the HB (see right panel of Figure 8) supports its membership to Peg III. On the contrary, V2 lies within 10 $r_{hl}$ (the star was identified in the data set of CCD1) and is about 0.3 mag above the HB level (see right panel of Figure 8), thus casting doubts on the actual membership to Peg III of this variable. We discuss V2 more in detail in Section 7.

| HJD (−2,457,000) | B (mag) | $\sigma_B$ (mag) | HJD (−2,457,000) | V (mag) | $\sigma_V$ (mag) |
|------------------|--------|----------------|------------------|--------|----------------|
| 335.60833        | 21.7788| 0.040          | 335.60828        | 21.3891| 0.0297         |
| 335.62004        | 21.8276| 0.036          | 335.61999        | 21.4334| 0.0275         |
| 335.63116        | 21.9492| 0.030          | 335.63109        | 21.5478| 0.0248         |
| 335.63837        | 22.1282| 0.045          | 335.63831        | 21.5708| 0.0270         |
| 335.65506        | 22.1653| 0.065          | 335.655          | 21.6142| 0.0300         |
| 334.58568        | 22.2208| 0.026          | 334.58562        | 21.7106| 0.0180         |
| 334.59818        | 22.5726| 0.039          | 297.7517         | 21.7876| 0.0213         |
| 334.60584        | 22.5909| 0.052          | 334.59814        | 21.8667| 0.0199         |

Note. The table is published in its entirety in the electronic edition of the journal. A portion is shown here for guidance regarding its form and content. (This table is available in its entirety in machine-readable form.)

Figure 2. Map of the sources measured in the LBC FOV of Psc II with respect to the galaxy center coordinates. Only sources selected according to the cuts described in Section 8 are displayed. Five blue ellipses are drawn showing from 1 (inner ellipse) to 5 times the galaxy $r_{hl}$ (outer ellipse; that is where V4, the outermost variable of Psc II, is located), adopting the position angle, $r_{hl}$, ellipticity, and center coordinates of Sand et al. (2012). A magenta filled square marks the fundamental-mode RRL (V1), a cyan filled triangle the confirmed SX Phe star (V3), and a red filled circle the RRab/AC star (V4). Red open circles show seven members of Psc II spectroscopically confirmed by Kirby et al. (2015).

5. Distance to Psc II and Peg III

We measured the distance to Psc II using V1, the bona fide RRab star located within the galaxy $r_{hl}$. The intensity-averaged V magnitude of V1 is $\langle V \rangle = 21.890 \pm 0.038$ mag (see Table 5), which we dereddened using a standard extinction law $A_V = 3.1 \times E(\text{B} - \text{V})$ and the reddening value from Schlafly & Finkbeiner (2011), $E(\text{B} - \text{V}) = 0.056 \pm 0.052$ mag. Similar to the other nine UFDs studied by our team (e.g., Dall’Ora et al. 2006; Greco et al. 2008; Clementini et al. 2012; Garofalo et al. 2013, and references therein), we adopted an absolute magnitude $M_V = 0.54 \pm 0.09$ mag for RRLs with a metallicity of $[\text{Fe/H}] = -1.5$ dex (Clementini et al. 2003) and the slope of the luminosity—metallicity relation provided by Clementini et al. (2003) and Gratton et al. (2004), namely, $\Delta M_V = 0.214 \pm 0.047$ mag dex$^{-1}$. However, later in the section we consider also more recent calibrations of the absolute magnitude of RRLs that are based on Gaia parallaxes.

A metallicity for V1 to enter the RRL luminosity—metallicity relation could in principle be obtained from the relation existing between the metal abundance ([Fe/H]), the period, and the $\phi_3$ parameter of the Fourier decomposition of the $V$-band light curve of RRab stars (Jurcsik & Kovacs 1996). However, this relation cannot be used here because the $V$-band light curve of Psc II-V1 (as well as that of Peg III-V1) does not satisfy the regularity conditions (Jurcsik & Kovacs 1996;}

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5 An independent estimate of reddening can be obtained for V1 using the Piersimoni et al. (2002) method for RRLs. From V1 we obtained a reddening value $E(\text{B} - \text{V}) = 0.052 \pm 0.023$ mag, which agrees very well with the reddening from Schlafly & Finkbeiner (2011).
Cacciari et al. 2005) that allow for a reliable application of this method. For the metallicity of Psc II we thus adopt the value \( [\text{Fe}/\text{H}] \sim -1.7 \pm 0.1 \) dex, which corresponds to the metal abundance of the theoretical isochrones best fitting the galaxy CMD (see Figure 9, Section 8), despite that the spectroscopic metallicity estimated by Kirby et al. (2015) is much lower (\( [\text{Fe}/\text{H}] = -2.45 \pm 0.07 \) dex). The distance modulus we derived for Psc II is then \( (m-M)_0 = 21.22 \pm 0.14 \) mag, which corresponds to a distance of \( d = 175 \pm 11 \) kpc. If we assume instead the Kirby et al. (2015) spectroscopic metallicity, the distance modulus would be 0.16 mag longer, placing Psc II \( \sim 14 \) kpc farther than our previous estimate. Within their respective errors, both these estimates are consistent with the Sand et al. (2012) distance of \( 183 \pm 15 \) kpc, which is about in the middle of our estimates.

The Gaia second data release in spring 2018 (Gaia DR2; Gaia Collaboration et al. 2018) published trigonometric parallaxes for more than 100,000 sources classified as RRLs. We have adopted the luminosity–metallicity relations from Muraveva et al. (2018), which are calibrated on a sample of

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**Table 5**

| Name   | R.A. (J2000) | Decl. (J2000) | Type    | \( P \) (days) | Epoch (max) HJD (2,457,000) | \( \langle B \rangle \) (mag) | \( A_B \) (mag) | \( \langle V \rangle \) (mag) | \( A_V \) (mag) | \( [\text{Fe}/\text{H}]^a \) (dex) |
|--------|--------------|---------------|---------|----------------|-----------------------------|-----------------------------|--------------|-----------------------------|--------------|-----------------------------|
| Psc II |              |               |         |                |                             |                             |              |                             |              |                             |
| V1     | 22:58:29.858 | +5:57:10.92   | RRab    | 0.5551         | 296.71                      | 22.28                       | 0.94         | 21.89                       | 0.69         | \( > -1.6 \) / \( -1.7 \)     |
| V2     | 22:58:33.355 | +5:57:43.63   | SX Phe(?) | 0.04905        | \ldots                        | \ldots                      | \ldots       | \ldots                      | \ldots       | \ldots                      |
| V3     | 22:58:40.807 | +5:56:23.16   | SX Phe   | 0.06348        | 333.6245                     | 24.245                      | 1.119        | 23.935                      | 0.775        | \ldots                      |
| V4RRL  | 22:58:44.659 | +5:54:16.33   | RRab    | 0.722          | 335.565                     | 21.98                       | 1.18         | 23.635                      | 0.93         | \( > -2.3 \)                  |
| V4AC   | 22:58:44.659 | +5:54:16.33   | AC      | 0.4186         | 335.612                     | 22.004                      | 1.097        | 21.635                      | 0.825        | \ldots                      |
| Peg III|              |               |         |                |                             |                             |              |                             |              |                             |
| V1     | 22:24:18.312 | +5:22:17.78   | RRab    | 0.5537         | 357.560                     | 22.58                       | 1.18         | 22.13                       | 0.96         | \( > -1.6 \) / \( -1.7 \)     |
| V2RRL  | 22:24:01.932 | +5:25:45.52   | RRab    | 0.6594         | 296.771                     | 22.33                       | 1.26         | 21.80                       | 1.16         | \( > -2.3 \)                  |
| V2AC   | 22:24:01.932 | +5:25:45.52   | AC      | 0.3972         | 357.531                     | 22.37                       | 1.03         | 21.85                       | 0.84         | \ldots                      |

**Note.**

^a From the CMD analysis (see Sections 7 and 8).
381 Galactic RRLs with Gaia DR2 parallax measurements, to estimate the distance to Psc II (and Peg III). Gaia parallaxes are known to be affected by a global zero-point offset with a mean value $\Delta \varpi_0 = -0.03$ mas DR2 (Lindegren et al. 2018; Arenou et al. 2018) and varying as a function of color, magnitude, and sky position of the sources. For the RRLs the Gaia DR2 parallax offset ranges from $-0.030$ to $-0.057$ mas (Muraveva et al. 2018). We summarize in Table 6 estimates of the distance modulus for Psc II (upper and middle portions of the table) and Peg III (lower portion), using the bona fide RRL in each galaxy and different choices for the absolute magnitude of RRLs. In particular, the estimates based on Gaia parallaxes are taken from the relations in Muraveva et al. (2018) with parallax offset $\Delta \varpi_0 = -0.03, -0.057$ (value fixed by Muraveva et al. 2018) to infer the linear $M_V - [\text{Fe/H}]$ relation using a subsample of 23 RRLs with metallicity from high-resolution spectroscopy and $-0.062$ mas (this is the highest offset value considered by Muraveva et al. 2018 when fitting the linear $M_V - [\text{Fe/H}]$ relation). Assuming $[\text{Fe/H}] = -1.71 \pm 0.1$ dex for V1 in Psc II, we obtained $(m - M)_0 = 21.12 \pm 0.18$ mag for both $\Delta \varpi_0 = -0.057$ mas and $\Delta \varpi_0 = -0.062$ mas. These distance moduli place Psc II closer than we find by adopting the Clementini et al. (2003) relation, but they are all still compatible within the errors. There is excellent agreement instead between the distance modulus from the Clementini et al. (2003) relation and the value $(m - M)_0 = 21.25 \pm 0.18$ mag obtained using the Muraveva et al. (2018) relation with mean offset of $-0.03$ mas (see upper portion of Table 6). Adopting the lower mean metallicity ([Fe/H] $= -2.45 \pm 0.07$ dex) spectrophotically determined by Kirby et al. (2015) (middle portion of Table 6), we get identical results using the Clementini et al. (2003) relation and the Muraveva et al. (2018) relation with parallax offset of $-0.057$ mas. These values are also in good agreement with the Sand et al. (2012) estimation. Finally, distance moduli from Muraveva et al. (2018) relations with $\Delta \varpi_0 = -0.03$ and $\Delta \varpi_0 = -0.062$ place Psc II, respectively, farther or closer than we find by adopting the Clementini et al. (2003) relation, but they are all still compatible within the errors.

Likewise, to estimate the distance to Peg III, we have used the intensity-averaged V magnitude of V1 ($(\bar{V}) = 22.126 \pm 0.031$ mag; see Table 5), the RRL with a firm classification, which was dereddened using the reddening value $E(B-V) = 0.126 \pm 0.003$ mag from Schlafly & Finkbeiner (2011) maps. Then, following the procedure applied for Psc II, we have adopted for the star the metal abundance $[\text{Fe/H}] = -1.6 \pm 0.20$ dex, corresponding to the metallicity of the theoretical isochrones best fitting the Peg III CMD (see right panel of Figure 9). This metallicity is significantly higher than the spectroscopic estimates by Kim et al. (2016) for the kinematically confirmed members of Peg III, which are as low as $[\text{Fe/H}] = -2.55 \pm 0.15$ dex; hence, we have used both metallicity values to estimate the distance to Peg III. We find the distance modulus $(m - M)_0 = 21.21 \pm 0.23$ mag ($d = 174 \pm 18$ kpc) adopting for V1 the metal abundance from the isochrone fitting and $(m - M)_0 = 21.42 \pm 0.19$ mag ($d = 192 \pm 16$ kpc) using the spectroscopic metal abundance from Kim et al. (2016). Both values are shorter than the literature value of $215 \pm 12$ kpc; however, the latter is consistent with the literature within the errors. Finally, as done for Psc II, we estimated the distance modulus of Peg III from Muraveva et al. (2018) luminosity–metallicity relations and

![Figure 4. Map of the sources measured in the LBC FOV of Peg III with respect to the galaxy center coordinates. Only sources selected according to the cuts described in Section 8 are displayed. We have marked the position of the two confirmed variables using a red filled circle for the RRab star (V1) and a red open circle for V2. We also show the spectroscopically confirmed members (blue stars) and an ambiguous member (orange star) according to Kim et al. (2016). Five green ellipses were drawn convolving the Peg III center coordinates, ellipticity, position angle, $r_9$, and its multiples, according to the values provided by Kim et al. (2016). The five ellipses correspond to 1, 2, 3, 5, and 10 times the $r_9$ of Peg III.](image-url)
three values ($\Delta \varpi_0 = -0.03, -0.057,$ and $-0.062$ mas, respectively) of the Gaia parallax offset (lower portion of Table 6). Again, we find that all estimates are consistent within their admittedly large errors, the Gaia parallax zero-point offsets $-0.057$ and $-0.062$ mas put Peg III closer than the value obtained from the Clementini et al. (2003) relation, and the best agreement is found for $\Delta \varpi_0 = -0.03$, which leads to $(m - M)_V = 21.24 \pm 0.25$ mag.

To ease the comparison with our previous studies of RRLs in UFDs, in the following sections we use for the distance moduli of Psc II and Peg III the estimates derived using the Clementini et al. (2003) relation.

### 6. Bailey Diagram and Oosterhoff Classification

We have used the V-band amplitudes and the periods of the bona fide RRab stars we have identified in Psc II and Peg III, to plot the stars on the period–amplitude diagram (blue circles and red stars in Figure 5, respectively) and make a comparison with the RRLs in other MW UFDs.

The RRLs detected in 21 other MW UFDs are also plotted in Figure 5 using different symbols: Coma Berenices (Musella et al. 2009; Vivas et al. 2020), Bootes I (Dall’Ora et al. 2006; Vivas et al. 2020), Bootes II and Bootes III (Sesar et al. 2014; Vivas et al. 2020), Canes Venatici I (Kuehn et al. 2008), Canes Venatici II (Greco et al. 2008), Carina II (Torrealba et al. 2018), Gru I and Gru II (Martínez-Vázquez et al. 2019), Leo IV (Moretti et al. 2009), Leo V (Medina et al. 2017), Hercules (Musella et al. 2012; Garling et al. 2018), Hydra II (Vivas et al. 2016), Hydrus I (Koposov et al. 2018; Vivas et al. 2020), Leo T (Clementini et al. 2012), Phoenix II (Martínez-Vázquez et al. 2019), Segue II (Boettcher et al. 2013), Sagittarius II (Joo et al. 2019), Tucana II (Vivas et al. 2020), Ursa Major I (Garofalo et al. 2013), and Ursa Major II (Dall’Ora et al. 2012; Vivas et al. 2020). In the Bailey diagram fundamental-mode and first-overtone RRLs lay well separated. As expected for their periods, the RRLs we have identified in Psc II and Peg III fall in the region of the fundamental-mode pulsators. In Figure 5 we have highlighted with solid lines the loci of the two Oosterhoff types, Oo I and Oo II, taken from Clement & Rowe (2000). The two bona fide RRab stars in Psc II and Peg III fall on/close to the Oo I line on the Bailey diagram. This is consistent with the metallicity we have inferred for these two RRLs from the isochrone fitting. Conversely, Psc II-V4 and Peg III-V2 both fall slightly beyond the Oo II locus when adopting for them the same periods as RRLs. It is clear from Figure 5 that UFDs display a large dispersion in the period–amplitude diagram. However, what seems to be unique of Psc II and Peg III is the sharp separation between Oo I and Oo II types of the two RRLs each of these UFDs contains (under the assumption that Psc II-V4 and Peg III-V2 are indeed RRLs; see Section 7). This seems to differ from what is generally found for other MW UFDs, whose RRLs tend either to lay preferentially between the two Oo lines, like in CVn I (the system that more closely resembles the classical MW dSphs), or to stay closer to just one of them, often the Oo II locus (as in Hercules, Phoenix II, Gru I, Coma Berenices, and CVn II).

### 7. The Intriguing Cases of V4 in Psc II and V2 in Peg III

As anticipated in Section 4, V4 in Psc II and V2 in Peg III have an uncertain classification. The B and V data of V4 can also be folded with $P \sim 0.72$ days and the variable being an RRab star (as well as for V2 in Peg III with $P \sim 0.66$ days), or with $P \sim 0.42$ days and the star being a first-overtone AC (as well as for V2 in Peg III with $P \sim 0.40$ days). ACs have been identified in a number of UFDs (i.e., CVn I, Kuehn et al. 2008; Hercules, Musella et al. 2012; Leo T, Clementini et al. 2012; Hydra II, Vivas et al. 2016). From an evolutionary point of view ACs can be associated with low metal abundance ([Fe/H] $\lesssim -1.4$ dex), intermediate-age (1–2 Gyr) stellar populations, but neither Psc II nor Peg III shows signs of intermediate-age population in their CMDs (see Section 8). However, ACs can also be formed by a binary evolution channel. In this case they would not trace a recent star formation episode, but would rather be the product of binary interaction that occurred about 1 Gyr ago (Gautschy & Saio 2017). This formation channel could justify the presence of ACs in systems hosting exclusively old stellar components like Galactic GCs and most of the MW UFDs. We have performed a number of tests to investigate the nature of Psc II-V4 and Peg III-V2. In particular, we have compared them with the PL and PW relations of ACs in the Large Magellanic Cloud (LMC) and with stellar evolutionary tracks for the typical mass and metallicity of ACs. These comparisons are presented in Appendix A. They lead us to rule out a classification of V4 and V2 as ACs belonging either to the Psc II and Peg III UFDs or to the field around them.

To explore whether V4 in Psc II and V2 in Peg III can be RRab stars with $P \sim 0.722$ and 0.656 days, respectively, we
start first from their position on the period–amplitude diagram (Figure 5). Both stars fall very close to the Oo II locus and have a higher luminosity and lower metallicity than the RRab stars Psc II-V1 and Peg III-V1, which lay instead near the Oo I locus. Variable stars in Oo II clusters have longer periods, higher luminosities, and lower metallicities than those in the Oo I clusters (see, e.g., Clement & Rowe 2000, and references therein) and are supposed to be evolved off the zero-age HB (ZAHB; see, e.g., Lee et al. 1990). All the properties of V4 and V2 are thus consistent with them being both RRab stars with Oo II characteristics and evolved off the ZAHB. However, as we have already pointed out in Section 6, although UFDs do show metallicity spreads as large as 1 dex among their members (see, e.g., Simon 2019, and references therein) and large dispersions in the period–amplitude diagrams of their RRLs (Figure 5), what makes Psc II and Peg III a rather remarkable case is their capability to host RRLs with such distinct Oo properties.

While it may prove difficult to explain how Psc II and Peg III managed to produce RRLs of both Oosterhoff types (but see Section 9), a further option may be that Psc II-V4 and Peg III-V2 belong to structures/stellar systems projected in front of their hosts. However, there is no sign of an overdensity/structure surrounding V4 in the isodensity contour maps of Psc II (see Figure 11). Moreover, the distance moduli inferred for Psc II-V1 and V4 appear to be well consistent with each other, within the errors. This is illustrated in Figure 6, which shows that stellar evolutionary tracks for 0.8 $M_\odot$ (a typical mass for RRLs) with metallicities corresponding to the metal abundance of V4 ($Z = 0.00005/\left[\text{Fe}/\text{H}\right] = -2.5$ dex, violet line; left panel) and V1 ($Z = 0.0044/\left[\text{Fe}/\text{H}\right] = -1.5$ dex, orange line; right panel), corrected for the distance modulus of Psc II inferred from V1, well fit the luminosity of both V4 and V1, hence supporting the conclusion that they are both members of Psc II.

Nevertheless, it remains unclear how the two stars can belong to the same system although they are about 8 kpc apart in projected distance (if we trust the difference in distance moduli; see Section 8) and about 5 $r_h$ apart from the center of Psc II.

On the other hand, all variables we have identified in this study are outside the $r_h$ of their hosts (except V1 in Psc II); therefore, we cannot rule out that they are field stars. Unfortunately, they are fainter than the Gaia limit ($G \leq 21$ mag; Gaia Collaboration et al. 2018); hence, no proper motions are available for them from Gaia to check their membership to Psc II and Peg III. However, we can evaluate the probability that they are indeed members of these UFDs by calculating how many field RRLs can be expected in the MW halo at the distance of Psc II and Peg III ($\sim 175$ kpc). Assuming the radial density distribution of RRLs in the Galactic halo derived by Medina et al. (2018), within 145 kpc from the Galactic center,
and considering that these authors have identified 13 RRLs beyond 130 kpc over 120 deg², we found that the number of MW halo RRLs expected at ∼175 kpc in 0.15 deg² (∼the LBT FOV) is lower than 10⁻⁵. Therefore, if V4 in Psc II and V2 in Peg III are indeed RRLs, their membership to the corresponding host galaxy is very much plausible.

To conclude, the most likely hypothesis is that Psc II-V4 and Peg III-V2 are RRab stars with Oo II characteristics belonging to, respectively, the Psc II and Peg III UFDs. However, it remains to clarify how Psc II (and Peg III) can host two stellar populations of different age and metallicity. May two separate star formation episodes have occurred in such small galaxies? This is not quite a common scenario among the MW UFDs (Bland-Hawthorn et al. 2015; Romano et al. 2015, and references therein). We also point out that metallicity is not the only factor that may cause the difference in luminosity among the RRab stars in these galaxies. Other contributors may be evolutionary effects, photometric errors, and, in particular, uneven sampling of the light curves. Only the collection of new observations allowing us to definitively pin down the period and classification in type of V4 and V2 may help us clarify this issue. Adding new data would also help to better constrain the period, amplitude, and mean magnitude of the other variable stars we have identified in these UFDs, hence strengthening their classification.

8. Color–Magnitude Diagrams of Psc II and Peg III

The V, B – V CMDs of Psc II and Peg III obtained in this study have already been introduced briefly in Section 7. We now discuss how they were derived and show them side by side in Figures 7 and 8 to ease their comparison.

To clean the lists of sources measured in each galaxy, we have used the quality information provided by the DAOPHOT quality image parameters χ and Sharpness. Only the stellar detections satisfying the photometric quality criteria −0.4 ≤ Sharpness ≤ 0.4 and χ < 2.2 in both B and V images were retained in the CMDs. This allowed us to reduce the contamination by background galaxies. In Figure 7 we have plotted all the stellar detections in the LBT FOV for each galaxy, selected according to the above χ and Sharpness values and separated according to the four CCDs of the LBC mosaic. We note that MW stars dominate the CMDs in Figure 7 for colors redder than B − V ∼ 1.6 mag. In order to better identify stars belonging to the Psc II galaxy, we have cross-matched our catalog against the Kirby et al. (2015) list of spectroscopically confirmed members of Psc II. All seven RGB stars that are Psc II members according to Kirby et al. (2015) have a counterpart in our catalog. They are marked by red open circles in the left panels of Figure 7. A magenta square marks V1, the bona fide RRab star, a red filled circle marks V4, the variable with less certain classification, both plotted according to their intensity-averaged mean magnitudes computed along the pulsation cycle. A cyan filled triangle shows the SX Phe star (V3). Similarly, in the right panels of Figure 7, the two variables identified in Peg III, V1 and V2, are marked by filled and open red circles, respectively, and plotted according to their intensity-averaged mean magnitudes and colors, the spectroscopically confirmed members by Kim et al. (2016) are marked by blue stars, and an orange star symbol marks the source whose membership is uncertain. Since the ambiguous member lies on the HB region, Kim et al. (2016) speculated that it might be an RRL. Based on our checks of the variability indices in B and V and the visual inspection of the light curves, we rule out that this star varies.

Our CMDs of Psc II and Peg III are rather deep, reaching V ∼ 26.5 mag; hence, they allow us to trace for each galaxy the main sequence (MS) below the turn-off (TO) point, which is located approximately between 25 and 25.5 mag in V, according to the theoretical isochrones overlaid on the CMDs (see Figure 9, later in this section).
As shown by the left panels of Figure 7, the Psc II galaxy is entirely contained in CCD2, the central CCD of the LBC configuration, where all the spectroscopically confirmed members and the variable stars we have identified in Psc II are located. Only in CCD2 is a hint of the galaxy HB and RGB recognizable (for the latter, the eye is guided by the spectroscopic members). The CMD of Psc II within the half-light radius is very poorly populated; only V1 and one of the seven
spectroscopic members are within the galaxy $r_{\text{g}}$; the other six confirmed members are located in the region between 1 and 4 times the galaxy $r_{\text{g}}$. We have tried to build a final CMD reasonably well populated, which contains all spectroscopic members and the variable stars in the field of Psc II. This is presented in the left panel of Figure 8, which shows all stellar sources located within 5 times the $r_{\text{g}}$ of the galaxy (all the CMDs shown in the remaining of this section correspond to sources within 5 $r_{\text{g}}$).

The Peg III UFD is also very small in size ($r_{\text{g}} = 53 \pm 1.4$ pc; Kim et al. 2016). As shown by Figure 4, the bona fide RRab star (V1) and the variable of uncertain classification are located, respectively, within 5 and 10 times the galaxy $r_{\text{g}}$, whereas the spectroscopic members are all within 3 $r_{\text{g}}$. Since both spectroscopic members and variable stars are rather far away from the center of Peg III, even more than for Psc II, the CMD we show in the right panel of Figure 8 contains all stars within 10 times the $r_{\text{g}}$ of Peg III. Furthermore, unlike Psc II, Peg III seems to be not entirely contained in CCD2, as one would expect given its spectroscopic members are within the galaxy.

The Peg III UFD is also very small in size ($r_{\text{g}} = 53 \pm 1.4$ pc; Kim et al. 2016). As shown by Figure 4, the bona fide RRab star (V1) and the variable of uncertain classification are located, respectively, within 5 and 10 times the galaxy $r_{\text{g}}$, whereas the spectroscopic members are all within 3 $r_{\text{g}}$. Since both spectroscopic members and variable stars are rather far away from the center of Peg III, even more than for Psc II, the CMD we show in the right panel of Figure 8 contains all stars within 10 times the $r_{\text{g}}$ of Peg III. Furthermore, unlike Psc II, Peg III seems to be not entirely contained in CCD2, as one would expect given its small size. V1 and the center coordinates of Peg III are within CCD2, whereas V2 is within CCD1. The most recognizable features in the CMDs of Psc II and Peg III are: (i) the HB at $V \sim 22$ mag (as also inferred from the mean magnitude of the bona fide RRab star in each UFD) populated by a few stars close to the red and blue edges of the RRL and roughly ending at $B-V \sim 0.2$ mag; and (ii) the RGB between $(B-V) \sim 0.7$ and $\sim 1.4$ mag, reaching as bright as $V \sim 19.5$–19 mag, which is disentangled thanks to the RGB member stars by Kirby et al. (2015) for Psc II and Kim et al. (2016) for Peg III. Additionally, in the CMD of Peg III a possible hint of asymptotic giant branch (AGB) or red horizontal branch (RHB) population can be recognized, as also suggested by Kim et al. (2016), thanks to three kinematic members brighter than the HB and bluer than the RGB (colors $0.6 < (B-V) < 0.8$ mag).

These features are indicative of a stellar population older than 10 Gyr in both Psc II and Peg III, in agreement with the typical ages of the stellar components observed in other MW UFDs. In order to estimate the age and metallicity of the Psc II and Peg III dominant stellar populations, we have overlapped on the CMDs the PARSEC stellar isochrones from Bressan et al. (2012), available on the CMD 2.9 web interface. The left panel of Figure 9 shows the CMD of Psc II in a region within 5 times the galaxy $r_{\text{g}}$ with overlaid the PARSEC isochrones for a fixed age of 13 Gyr (the best fit we have obtained) and five different values of metallicity: $[\text{Fe/H}] = -2.3, -1.9, -1.8, -1.7$, and $-1.5$ dex. The isochrones were adjusted to the distance modulus of Psc II (21.22 mag, as inferred from V1, the bona fide RRab star within the galaxy $r_{\text{g}}$) and a reddening value of $E(B-V) = 0.056$ mag from the Schlafly & Finkbeiner (2011) maps and a distance modulus of $21.21 \pm 0.32$ mag, as inferred from the bona fide RRab star in Peg III (V1). The isochrones that better reproduce the RGB and the HB level along with the position of Peg III-V1 are those for metallicities between $-1.7$ and $-1.6$ dex; however, the isochrone with $[\text{Fe/H}] = -1.6$ dex does not reproduce the overall extension of the HB, which, instead, is well covered by the $[\text{Fe/H}] = -1.7$ dex isochrone. The metallicity we find from the isochrone fitting is much higher than the value inferred by Kim et al. (2016) applying the same technique. Using isochrones from Dotter et al. (2008), Kim et al. (2016) suggest as the best-fit isochrone for Peg III the one with an age of 13.5 Gyr and metallicity $[\text{Fe/H}] = -2.5$ dex. However, we think that the isochrone set with higher metallicity ($[\text{Fe/H}] = -1.5$ dex; right panel of Figure 2 in Kim et al. 2016) better reproduces also the CMD by Kim et al. (2016).

In summary, our results from the CMD isochrone fitting suggest that both Peg III and Psc II host a stellar population more metal-rich than derived from spectroscopically confirmed members or by isochrone fitting in previous works. Among the MW UFDs, only Leo T (Clementini et al. 2012) and Ursa Major II (Dall’Ora et al. 2012) have a similarly high metallicity. On the other hand, the comparison with isochrones of different metallicity presented here, the very low metallicity measured for the spectroscopically confirmed members, and the position on the period–amplitude diagram also suggest a plausible scenario where V4 in Psc II and V2 in Peg III are very metal-poor ($[\text{Fe/H}] > -2.4$ dex) RRab members and tracers of a very metal-poor component of these UFDs.

Indeed, as we have shown in Section 5, if we adopt for V4 in Psc II the metallicity derived by Kirby et al. (2015; $[\text{Fe/H}] = -2.45 \pm 0.07$ dex), the inferred distance modulus is $(m - M_0) = 21.12 \pm 0.20$ mag, which would be consistent, within the errors, with the distance modulus inferred from the more metal-rich RRab star V1 (21.22 \pm 0.14 mag). In the same vein, if V2 is a very metal-poor ($[\text{Fe/H}] = -2.54 \pm 0.79$ dex) RRab star belonging to Peg III, its distance modulus (21.07 \pm 0.42 mag) would be consistent, within the errors, with the distance modulus inferred from the more metal-rich RRab star V1 in Peg III (21.21 \pm 0.32 mag).

Such very metal-poor stellar components as those possibly traced by V4 in Psc II and V2 in Peg III should be associated with steep RGBs in the CMDs. Unfortunately, there is no clear sign of such a metal-poor RGB, steeper than the metal-rich RGB associated with V1, in the CMD of Psc II (see left panels of Figures 7 and 8). However, the bright portion of the Psc II CMD is so scarcely populated that even the metal-rich RGB would hardly be recognized if there were not the spectroscopically confirmed members to guide the eye. Conversely, a metal-poor RGB, steeper than the metal-rich RGB associated with V1, can be recognizable in the CMDs of Peg III (see right panels of Figures 7 and 8).

As both the PARSEC isochrones (CMD 2.9 web interface) and the isochrones by Pietrinferni et al. (2004, BaSTI web interface) do not reach metallicities lower than $[\text{Fe/H}] \sim -2.5$ dex, we have tried to investigate what may be causing these discrepant results by exploring different sets of isochrones including also alpha-enhancement, since UFDs are expected to have enhancement of alpha-elements. In particular, in Appendix B, we have considered Dotter et al. (2008) isochrones (available at http://stellar.dartmouth.edu/models/).

5 http://stev.oapd.inaf.it/cmd

6 http://basti.oa-teramo.inaf.it/BASTI/WEB_TOOLS/IM_HTML/index.html
−2.2/−2.3 dex, as a last check, we compared the CMDs of Psc II and Peg III to the mean ridgelines of metal-poor Galactic GCs. The left panel of Figure 10 shows the mean ridgelines of Psc II and Peg III to the mean ridgelines of metal-poor Galactic GCs. The left panel of Figure 10 shows the mean ridgelines of the Galactic GCs used to fit the RGB (with V1 and Kirby et al. 2015 spectroscopic members as references) and the HB (with V1 and V4 as references) of the two different populations possibly observed in Psc II. Specifically, we used the fiducial tracks published by Piotto et al. (2002) for M15 and NGC 5824, which have metallicities of [Fe/H] = −2.4 and −1.9 dex, respectively, to fit the metal-poor component, and the fiducial lines of M13 and M5, with metallicities of [Fe/H] = −1.5 and −1.3 dex, respectively, to fit the metal-rich component in Psc II. The ridgelines were corrected according to the proper reddening and distance modulus of each GC (Harris 1996'), $E(B-V) = 0.1$ mag and $(m-M)_{V} = 15.39$ mag for M15, $E(B-V) = 0.13$ mag and $(m-M)_{V} = 17.94$ mag for NGC 5824, $E(B-V) = 0.02$ mag and $(m-M)_{V} = 14.33$ mag for M13, $E(B-V) = 0.03$ mag and $(m-M)_{V} = 14.46$ mag for M3, and then further shifted to the distance modulus (21.22 ± 0.14 mag) and reddening $E(B-V) = 0.056 ± 0.052$ mag (Schlafly & Finkbeiner 2011) of Psc II. The ridgeline of NGC 5824, corresponding to a metallicity of [Fe/H] = −1.9 dex, well traces the RGB and the position of V4, while M5 and M13 well reproduce the RGB and the position of V1. We conclude that Psc II might host two old stellar components, a metal-poor component ([Fe/H] > −2.3 dex), traced by V4, and a higher-metallicity component traced by V1 ([Fe/H] > −1.6/1.7 dex). Totally similar results are found by overplotting the ridgelines of the same GCs to the CMD of Peg III. This is shown in the right panel of Figure 10, where we have assumed for Peg III the distance modulus inferred from the RRab star (V1). As done for Psc II, to fit the HB defined by V1 and the RGB of the metal-rich component, we used the fiducial lines of M13 and M5, while the RGB and HB of the metal-poor component are well traced by the fiducial lines of M15, corresponding to a metallicity of [Fe/H] = −2.4 dex. The fit of the Peg III CMD with the GC ridgelines confirms the results and the metallicities suggested by the fit with the theoretical isochrones, thus leading us to conclude that also Peg III might host two old stellar components with different metallicity, a higher-metallicity component traced by V1 and a metal-poor component traced by V2.

9. On Metal Retention in Psc II and Peg III

In this section we discuss how small systems like Psc II and Peg III may have managed to form stars with such a large dispersion on the metallicity distribution as Kirby et al. (2015) measured in Psc II ($\sigma_{[\text{Fe/H}]} = 0.48_{-0.29}^{+0.70}$), a spread that is confirmed by our isochrone fitting of the CMDs (see Section 8) and the properties of the variable stars we have identified in these two galaxies.

The present-day stellar masses ($M_*$) of Psc II and Peg III can be derived by their absolute $V$-band magnitudes (Table 2) and from the stellar mass-to-light ratio of a low-metallicity stellar population, which at an age of $\sim$10 Gyr is of the order of $\sim$2.73 (Bruzual & Charlot 2003) assuming a Salpeter (1955) stellar initial mass function (IMF). With these assumptions and for a solar $V$ magnitude $M_V = 4.83$ mag, one obtains $M_* = 10,000$ and $M_*$ $\sim$5300 $M_\odot$ for Psc II and Peg III, respectively. These stellar mass values lie at the lower end of the values found for Local Group dwarf galaxies (e.g., Kirby et al. 2013).

These assumptions imply that each of them must have hosted $\sim 10^2$ massive stars (adopting the stellar mass of Peg III as a reference value and again assuming a Salpeter IMF) and possibly a number of core-collapse supernovae (SNe) of the same order of magnitude must have exploded throughout their history. Assuming that each SN has produced $\sim 0.1 M_\odot$ of Fe, this also implies that these stars must have synthesized and ejected in total $\sim 10 M_\odot$ in the form of Fe. Present-day stars show a spread in [Fe/H] of 0.3–0.6 dex, much larger than the

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Figure 10. Same as in Figure 8, but with solid lines showing the ridgelines of the Galactic GCs: M15 (cyan), NGC 5824 (blue), M13 (green), and M5 (orange).
one shown by stellar systems of comparable mass, i.e., GCs, which is commonly of the order of 0.1 dex (except a few cases such as ω Cen; Renzini et al. 2015). Similar large metallicity spreads (up to 0.5 dex) are common in other MW UFDs (e.g., Simon & Geha 2007).

This is likely to indicate that, at variance with most GCs and as for other UFDs, Psc II and Peg III were able to retain a significant amount of the metals produced by SNe and incorporate it into new stars. This fact seems to contrast with the idea that, despite the small number of massive stars hosted by each of the two systems, the total amount of energy released by such stars in the form of both stellar winds and SNe exceeds the binding energy of the gas. An order-of-magnitude estimate of the binding energy can be performed as

$$E_b = \frac{G M_{\text{gas}} M}{r_h},$$

where $M_{\text{gas}}$ is the gas mass present in the system when most of its stars formed, $G$ is the gravitational constant, and $M$ and $r_h$ are the total mass and half-light radius, respectively. Assuming that during star formation $M_{\text{gas}} \sim M_*$ and the data of Table 2 for the effective radii $r_h$ and for the dark matter halo mass of the two galaxies, one finds that in both cases one single SN would be enough to completely expel all the natal gas.

However, the requirement for the SN energy release to exceed the binding energy is a necessary but not sufficient condition to expel all the metal-rich gas from a bound system. One of the reasons is that the conversion efficiency of the energy injected by SNe into kinetic energy of the interstellar medium (ISM) is generally well below unity, since a considerable fraction is lost via radiative losses (e.g., Mori et al. 2002). Another important argument is related to the spatial distribution of massive stars. In a low-density system such as a dwarf galaxy, massive stars are likely to have formed in isolated associations, scattered within the entire extent of the host galaxy, with important consequences on the effects of their energetic feedback. Previous works have shown that if isolated SN explosions occur at random times, it is difficult to reach the conditions for the gas to be heated at high temperatures to generate a steady wind (Nath & Shchekinov 2013). This is mostly due to the difficulty of SN remnants to overlap and heat the gas at sufficient temperatures to achieve an outflow (typically $T > 10^8$ K). Massive stars are likely to have originated grouped in some OB associations, but in that case the feedback sources would be even more isolated throughout the volume over which the gas is distributed. In principle, the simultaneous action of the continuous winds blown by massive stars in the pre-SN phase produces interstellar bubbles that could merge in a short time and lead to a large porosity of the hot gas. This process has turned out to be efficient in particular in stellar clusters, where the relative distances between OB associations are of the order of $< 1$ pc, and these can act simultaneously to rapidly achieve a large thermalization efficiency of the ISM (Calura et al. 2015; Yadav et al. 2017; Silich & Tenorio-Tagle 2018). However, even in the case of sources acting simultaneously, an outflow will not always be driven. In fact, off-center feedback sources might drive inward-propagating shocks that compress the gas in the innermost regions, with the effect of enhancing the radiative losses (Mori et al. 2002; Romano et al. 2019).

It is worth noting that even in conditions in which a massive outflow cannot originate, the expulsion of metals produced by SNe is facilitated with respect to the cold gas, as metals are injected at high velocity and in a hot phase, in particular in the outskirts of a galaxy or when the density of the surrounding medium is low. However, given the low metallicity of the two systems, the retention of a very small amount of Fe is enough to originate the [Fe/H] spread. In fact, considering an initially metal-free system and an average present-day stellar metallicity of [Fe/H] = −2.3 in Peg III, it is sufficient to retain and incorporate into stars 0.05 $M_\odot$ of Fe, which corresponds to 0.5% of the total amount of Fe produced by Type II SNe, and presumably an even smaller fraction to account for a 0.6 dex spread in Fe.

It is worth noting that this estimate does not include the Fe released by Type Ia SNe, which explode on longer timescales than Type II SNe and in general release a larger amount of Fe (Maguire 2017).

The data set collected in this work does not allow us to assess the precise duration of the star formation episode that gave place to the stars of Peg III and Psc II. To derive this quantity, the collection of a larger sample of stars with measured Fe abundances is required, which will allow one to compute a metallicity distribution function. This quantity can be studied by means of chemical evolution models and, as it is known to depend on the infall timescale, can provide strong constraints on the duration of the star formation history (e.g., Vincenzo et al. 2019).
Figure 12. Isodensity contour maps of Peg III obtained with a bin size of 0''/23. Left: isodensity map from all stars in the photometric catalog of Peg III selected by $\chi$ and Sharpness parameters. Right panel: same as the left panel, but only for MS and RGB stars selected with the guidance of the theoretical isochrones. Peg II is located in the upper left direction on these maps. The color bar provides the number of $\sigma$ values above the background represented by each isodensity contour level. The isodensity contour levels in the maps of Peg III vary from 1.5$\sigma$ to 12$\sigma$ above the background.

10. Isodensity Contour Maps

Figure 11 shows the isodensity contour maps obtained from all stars in our photometric catalog of Psc II, selected by the $\chi$ and Sharpness conditions described in Section 8 and using the same limits as for the galaxy CMD. The selected stars have been binned adopting a bin size of 0''/23. The left panel shows the isodensity contour map obtained selecting only MS and RGB stars (1387 sources), the middle panel only HB stars (24 sources), and the right panel only RGB stars (309 sources). RGB, MS, and HB stars were selected with the guidance of the theoretical isochrones we have overlaid on the galaxy CMD, and to minimize the contamination by field sources, we considered only stars within 0.1 mag from the best-fitting isochrones. To quantify a possible contamination of our subsamples by MW stars, on the assumption that the MW stars are uniformly distributed over the whole LBT FOV, we have counted the number of sources in 1 arcmin$^2$ regions at about 10' in distance from the center of Psc II ($\geq 10 r_h$). This number corresponds to six sources, on average, which we can assume are all background/foreground objects. Since within an area of 1 arcmin$^2$ centered on Psc II we find 54 sources, we can conclude that at most $\sim$11% of the sources in our subsamples may be MW contaminants. On the other hand, since the MW stars dominate the reddest part of the CMD ($B - V \gtrsim 1.6$ mag; see Figure 8) and barely overlap with the Psc II RGB, MS, and HB stars, we can safely assume that background/foreground contamination is almost negligible in the isodensity contour maps in Figure 11.

All maps in Figure 11 confirm the presence of a stellar overdensity at their center, corresponding to the position of the Psc II galaxy. This overdensity is clearly seen also in the isodensities of the RGB-only and HB-only stars. The isodensity maps of Psc II do not show an irregular shape as one would expect if the galaxy were undergoing tidal disruption or were interacting with Peg III. For the sake of completeness, Peg III is located in the lower right direction on these maps.

Figure 12 shows the isodensity contour maps of Peg III obtained using the same bin size and selection of the sources by $\chi$ and Sharpness, as adopted for Psc II. The left panel corresponds to sources on the whole CMD (6557 stars), whereas the right panel corresponds to only MS+RGB stars selected by overlaying the theoretical isochrones on the CMD of Peg III (1125 sources). Both isodensity maps show an overdensity at the center, corresponding to the Peg III galaxy.

Other, more extended overdensities are visible in the maps in Figure 12. They are not real structures, but rather artifacts caused by regions with deeper exposures (see Figure 4) due to the LBT rotation discussed in Section 3. The main overdensity at the center of the map in the left panel of Figure 12 is clearly seen also in the isodensity map of the RGB and MS stars, while the fictitious overdensities have now almost disappeared. Similarly to Psc II, the isodensity maps of Peg III do not show an irregular shape. The regular shape of the Psc II and Peg III isodensity maps leads us to rule out the existence of a clear link or stellar stream between these two UFDs.

11. Conclusions

Using $B$, $V$ time-series photometry obtained with the LBCs at the LBT, we have performed the first study of the variable stars in the Psc II and Peg III UFDs and derived the main properties of their resolved stellar populations. We have focused on the comparison of the Psc II and Peg III properties, in order to investigate the existence of a physical connection between these two galaxies, which have a spatial separation of only $43 \pm 19$ kpc, as was suggested in previous studies (Kim et al. 2015, 2016). For this comparison we have used as main tools (i) the properties of the RRLs identified in the two systems, (ii) the features of the observed CMDs, and (iii) the density contour maps.

In Psc II we have identified four variable stars (upper portion of Table 5): an RRab star (V1) with $P \sim 0.56$ days, an SX Phoenicis star (V3; $P \sim 0.06$ days) lying within the $r_h$ of Psc II, and a third variable, V4, with uncertain classification and about 0.25 mag brighter than V1, which is outside the galaxy’s $r_h$. A fourth source within the $r_h$ of V2, shows variability only in the $B$ band with $P \sim 0.05$ days and was classified as a candidate SX Phoenicis star. The period and amplitude of the light variation place V1 on the OoI locus of the period–amplitude diagram. From the mean magnitude of V1 we measured a distance modulus of $21.22 \pm 0.14$ mag, which places Psc II at 175 $\pm 11$ kpc from us, in agreement, within the errors, with previous literature estimates and at the same distance as Peg III. The period of V4 is uncertain. The source could be either an RRab star with $P = 0.72$ days or a first-overtone AC with $P = 0.42$ days. However, from the comparison with theoretical isochrones overlaid on the galaxy CMD and the $PL$ and $PW$ relations for ACs and CCs in the LMC, we conclude that V4 is likely a metal-poor ([Fe/H] $\gtrsim -2.4$ dex) RRab star with Oo II
pulsation characteristics belonging to Psc II. The CMD suggests the presence in Psc II of a dominant old stellar population \( (t > 10 \text{ Gyr}) \) with metallicity \([\text{Fe/H}] > -1.8 \text{ dex}\), along with, possibly, a minor, more metal-poor component traced by Psc II-V4.

In Peg III we have identified two variable stars (lower portion of Table 5): an RRab star with \( P \sim 0.55 \text{ days} \) (V1), and a variable with uncertain type classification (V2). Both variables are located outside the galaxy \( r_h \), within \( 4r_h \) and \( 10r_h \), respectively, from the center of Peg III. Similarly to Psc II, the period and amplitude of the bona fide RRab star (V1) place the variable star close to the Oo I locus in the period-amplitude diagram (Figure 5). According to the distance modulus inferred from V1, \( 21.21 \pm 0.23 \text{ mag} \), Peg III is at \( 174 \pm 18 \text{ kpc} \), in good agreement with the literature and at the same distance from us as Psc II. V2 in Peg III has totally similar characteristics to V4 in Psc II. It could be either an RRab star with \( P \sim 0.66 \text{ days} \) or an AC with \( P \sim 0.40 \text{ days} \) and about 0.3 mag brighter than the galaxy HB. However, similar tests to those done for Psc II-V4 lead us to conclude that V2 is very likely an RRab star with Oo I II characteristics belonging to Peg III.

The comparison of the CMD with stellar isochrones suggests the presence also in Peg III of a dominant old stellar component (>10 Gyr) with metallicity larger than \([\text{Fe/H}] \sim -1.8 \text{ dex}\). However, the RGB of Peg III exhibits a non-negligible spread in color, indicative of a significant metallicity spread. This evidence, along with the pulsation properties of V2, indicates the presence in Peg III of an old, more metal-poor (\([\text{Fe/H}] \sim -2.4 \text{ dex}\)) stellar component, as also supported by the comparison with the mean ridgelines of Galactic GCs (see Figure 10).

In summary, Psc II and Peg III share not only very similar properties but also almost the same issues.

There are a number of alternative hypotheses that could explain why Psc II and Peg III have so many similar properties: (1) they could be the leftovers of the same large galaxy that entered the MW environment and was totally disrupted by a close encounter with our Galaxy some gigayears ago; (2) they could be satellites of one of the present-day MW dSph satellites or of a dSph that has been completely cannibalized by the MW; (3) they could be separate entities, which just by chance are close on the sky and share similar properties; and, finally, (4) they could have been born in a pair. However, in spite of all the similarities and the proximity on the sky, the density contour maps do not reveal signatures of a tidal interaction between them. If they were indeed born in a pair, or were physically connected in the past, no trace of this physical connection seems to have survived.

The analysis we have presented here revealed very intriguing characteristics and similarities of Psc II and Peg III, prompting us to further study these systems. Unfortunately, the HB of the two galaxies is at/below the limiting magnitude reached by Gaia (\( V \sim 20.5-21 \text{ mag} \); Gaia Collaboration et al. 2018), but their brighter RGB stars are well within the reach of Gaia. Psc II and Peg III are in a region of the sky still poorly sampled by the observations released in Gaia DR2. However, the Gaia sky coverage is rapidly increasing, and in future data releases Gaia will likely tell us whether Psc II and Peg III share the same relative proper motions. Furthermore, in the near future the Rubin Observatory Large Synoptic Survey Telescope (LSST), designed to collect deep (5 mag deeper than Gaia), ground-based, wide-field imaging from the blue to the near-infrared wavelengths, will be able to provide observations of Psc II and Peg III and the field between them deep enough to shed light on the nature and origin of this intriguing couple.

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Appendix A

Psc II-V4 and Peg III-V2 as Anomalous Cepheids

ACs are known to follow specific Period—Luminosity (PL) and Period—Wesenheit (PW) relations, which differ from both the classical and the Type II Cepheid relationships (Soszyński et al. 2008). Therefore, if V4 and V2 are ACs, they should conform to the PL and PW relations of ACs.

![Figure 13. PW relations (solid lines) for ACs (left panel; from Ripepi et al. 2014) and CCs (right panel; from Jacyszyn-Dobrzeniecka et al. 2016) in the LMC, transformed to the B and V bands. Dotted lines represent the 1σ uncertainties, which for the AC relations correspond to 0.15 mag and for the CCs to 0.10 mag. A red filled circle shows the position of V4, according to the period of ~0.42 days and a Wesenheit index calculated for a distance modulus of \( \mu = M_V = 21.22 \text{ mag} \) as estimated from V1, the RRL inside the half-light radius of Psc II. The blue filled circle shows V4 but adopting a mass of 1.8 \( M_\odot \), and a Wesenheit index calculated for a distance modulus of 22.4 mag.](image-url)
We have compared V4 with the PW relations followed by ACs in the LMC (see Ripepi et al. 2014). These relations are defined in the $V$ and $I$ bands; hence, we converted them to the $B$, $V$ bands\(^\text{10}\) using the relation $\langle W(V, I) \rangle = -0.22 (\pm 0.001) + 1.03 \langle W(B, V) \rangle$ (Equation (12) of Marconi et al. 2004).

The PW relations of the LMC ACs converted into $B$ and $V$ bands are shown as solid lines in the left panel of Figure 13, together with their 1σ uncertainties (dotted lines). In this figure the lower line is the PW relation for fundamental-mode ACs, while the upper line is for ACs that pulsate in the first-overtone mode. Psc II-V4 (red filled circle) is plotted according to the period as an AC and the Wesenheit index computed by correcting the star $\langle V \rangle$-band apparent magnitude for the distance modulus $(m - M)_0 = 21.22$ mag as estimated from $V1$, the RRab star within the $r_h$ of Psc II. V4 lies within the 1σ uncertainty of the PW relation for first-overtone ACs; hence, it could indeed be an AC belonging to Psc II. As a check, in the right panel of Figure 13 we have compared V4 also with the PW relations for LMC classical Cepheids (CCs) by Jacyszyn-Dobrzeniecka et al. (2016). The star appears to be significantly fainter than the Wesenheit index of a fundamental-mode CC with the same period; hence, it is unlikely that it could be a CC of Psc II. Furthermore, in the CMD of Psc II (see Figure 8) there is no indication of the presence of a young population ($< 500$ Myr) as that traced by CCs (for a detailed description of the Psc II CMD, and the Peg III CMD as well, we refer the reader to Section 8). Figure 13 seems thus to support the possibility that V4 might be a first-overtone AC of Psc II. We further checked this hypothesis comparing the star with stellar evolutionary tracks by Pietrinferni et al. (2004, available at http://bastian-teramo.inaf.it/index.html), for the typical mass and metallicity of ACs ($\sim 1.8-2.2 M_\odot$ according to Caputo et al. 2004 and $Z = 0.0004$ following Marconi et al. 2004).

This is illustrated in the three panels of Figure 14 that show the CMD of Psc II with overlaid evolutionary tracks for metallicity $Z = 0.0003$ and masses of 1.8, 1.9, and 2.0 $M_\odot$, corrected for the distance modulus of Psc II and for a reddening of $E(B-V) = 0.056$ mag according to Schlafly & Finkbeiner (2011).

This comparison shows that if V4 were indeed an AC belonging to Psc II, it should be at least 1 mag brighter to lie on the proper region of the evolutionary track: the hook above the HB. On the other hand, since V4 is at about $5r_h$ from the Psc II center, it could be a field AC. We thus shifted the stellar tracks so as to fit the luminosity of V4 and found that the hook of the 1.8 $M_\odot$ track would fit the luminosity of V4 for a distance modulus of $(m - M)_0 \sim 22.4$ mag and for longer moduli in the case of larger masses.

\(^{10}\)The Wesenheit index in our case is $W(B, V) = M_V - 3.1 \times (B - V)$, where $M_V$ is the $V$ magnitude corrected for the distance.
Figure 16. Stellar evolutionary tracks (BaSTI web interface) for 1.8, 1.9, and 2.0 $M_\odot$ (green solid line; left, middle, and right panels, respectively) and metallicity $Z = 0.0003$ ([Fe/H] $= -1.8$ dex) overlaid on the CMD of Peg III. The tracks were corrected adopting the distance modulus of Peg III derived from the RRab star (V1; $(m - M)_0 = 21.21$ mag) and the reddening $E(B - V) = 0.13$ from Schlafly & Finkbeiner (2011) maps. V2 is marked by a red open circle, the bona fide RRab star V1 by a red filled circle, and the spectroscopically confirmed members from Kim et al. (2016) by blue and orange stars.
However, adopting such longer distance moduli, V4 could no longer fit any of the PW relations for ACs or CCs, as clearly shown by blue filled circles in Figure 13. Based on these conflicting results, we conclude that the classification of V4 as an AC belonging either to Psc II or to the background field is very unlikely.\footnote{We have shown in Section 7 that the probability of finding field RRLs at the distance of Psc II and Peg III is very low. Finding MW field ACs at such distances is even less probable, because ACs are much rarer than RRLs. Indeed, within a region of 20,000 deg$^2$ covered by the Catalina Surveys Data Release-1, Drake et al. (2014) have identified a total number of only 64 candidate ACs, and a small fraction of them, no more than $\sim 0.01\text{–}0.015$, are distributed beyond Psc II and Peg III Galactic latitudes ($l > 65\degree$). Since the LBT FOV is more than $10^6$ times smaller than the area covered by Drake et al. (2014), the fraction of MW halo ACs at the Galactic latitude of Psc II and Peg III is approximately $9 \times 10^{-8}$.} Totally similar conflicting results were found also for V2 in Peg III (see Figures 15 and 16), leading us to rule out a classification as AC also for V2 in Peg III.

### Appendix B

**Dotter et al. 2008 Isochrones on the CMD of Psc II**

Figure 17 shows CMD of Psc II (same as the left panel of Figure 8) with overlaid Dotter et al. (2008) isochrones for different metallicities, $-2.5$, $-2.0$, and $-1.5$ dex, a fixed age (13.5 Gyr, left panels; 11 Gyr, right panels), and a fixed $[\alpha/Fe]$ enhancement of 0.2 dex in panel (a) and 0.6 dex in panel (b).

The best agreement between variable stars and spectroscopic metal-poor stars is achieved for an isochrone with metal abundance between $-2$ and $-1.5$ dex and rather old. Here, Dotter et al. (2008) isochrones with 13.5 Gyr seem to be quite consistent with the PARSEC isochrones of 13 Gyr we have used throughout the paper. In summary, results do not seem to change significantly by selecting different isochrone sets adopted as reference. On the other hand, the discrepancy with previous studies may also arise because the photometry in this paper is much deeper than in previous works.

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