Potential energy surfaces of actinide and transfermium nuclei from multi-dimensional constraint covariant density functional theories

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Abstract. Multi-dimensional constrained covariant density functional theories were developed recently. In these theories, all shape degrees of freedom $\beta_{\mu}$ deformations with even $\mu$ are allowed, e.g., $\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}, \beta_{40}, \beta_{42}, \beta_{44}$, and so on and the CDFT functional can be one of the following four forms: the meson exchange or point-coupling nucleon interactions combined with the non-linear or density-dependent couplings. In this contribution, some applications of these theories are presented. The potential energy surfaces of actinide nuclei in the $(\beta_{20}, \beta_{22}, \beta_{30})$ deformation space are investigated. It is found that besides the octupole deformation, the triaxiality also plays an important role upon the second fission barriers. The non-axial reflection-asymmetric $\beta_{32}$ shape in some transfermium nuclei with $N = 150$, namely $^{246}\text{Cm}$, $^{248}\text{Cf}$, $^{250}\text{Fm}$, and $^{252}\text{No}$ are studied.

1 Introduction

“Shape” gives an intuitive understanding of spatial density distributions of quantum many-body systems including atomic nuclei. For the description of the nuclear shape, it is convenient to use the following parametrization

$$\beta_{\mu} = \frac{4\pi}{3AR^2}(Q_{\mu}),$$

where $Q_{\mu}$ are the mass multipole operators. A schematic show of some typical shapes is given in Fig. 1\textsuperscript{[1]}. The majority of observed nuclear shapes is of spheroidal form which is usually described by $\beta_{20}$. Higher-order deformations with $\lambda > 2$ such as $\beta_{30}$ also appear in certain atomic mass regions\textsuperscript{[2]}. In addition, non-axial shapes in atomic nuclei, in particular, the nonaxial-quadrupole (triaxial) deformation $\beta_{22}$ have been studied both experimentally and theoretically\textsuperscript{[3,4,5]}. There is no a priori reason to neglect the nonaxial-octupole deformations, especially the $\beta_{32}$ deformation\textsuperscript{[6,7,8]}.

Furthermore, more shape degrees of freedom play important roles in the study of potential energy surfaces of atomic nuclei. Particularly, various shape degrees of freedom play important and different roles in the occurrence and in determining the heights of the inner and outer barriers in actinide nuclei (in these nuclei double-humped fission barriers usually appear). For example, the inner fission barrier is usually lowered when the triaxial deformation is allowed, while for the outer barrier the reflection asymmetric (RA) shape is favored\textsuperscript{[9,10,11,12,13]}. Nowadays, it becomes more and more desirable to have accurate predictions of fission barriers also for superheavy nuclei\textsuperscript{[14,15,16,17,18,19]}. It is usually customary to consider only the triaxial and reflection symmetric (RS) shapes for the inner barrier and axially symmetric and RA shapes for the outer one\textsuperscript{[15,20,21,22]}. The non-axial octupole deformations are considered in both the macroscopic-microscopic (MM) models\textsuperscript{[23]} and the non-relativistic Hartree-Fock theories\textsuperscript{[24]}.

In order to give a microscopic and self-consistent study of the potential energy surface with more shape degrees of freedom included, multi-dimensional constrained covariant density functional theories are developed recently\textsuperscript{[25,26]}. In these theories, all shape degrees of freedom $\beta_{\mu}$ deformations with even $\mu$ are allowed, e.g., $\beta_{20}, \beta_{22}, \beta_{30}, \beta_{32}, \beta_{40}, \beta_{42}, \beta_{44}$, and so on. In this contribution, we present two recent applications of these theories: the potential energy surfaces of actinide nuclei and the non-axial reflection-asymmetric $\beta_{32}$ shape in some transfermium nuclei. In Section 2, the formalism of our multi-dimensional constrained covariant density functional theories will be given briefly.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Fig1.png}
\caption{(Color online) A schematic show of some typical nuclear shapes: (a) sphere; (b) prolate spheroid; (c) oblate spheroid; (d) hexadecapole shape; (e) triaxial ellipsoid; (f) reflection symmetric octupole shape; (g) tetrahedron; (h) reflection asymmetric octupole shape with very large quadrupole deformation. Taken from Ref. [1].}
\end{figure}
The results and discussions are presented in Section 3. Finally we give a summary in Section 4.

2 Formalism

The details of the formalism for covariant density functional theories can be found in Refs. [27,28,29,30,31,32]. The CDFT functional in our multi-dimensional constrained calculations can be derived from the following four forms: the meson exchange or point-coupling nucleon interactions combined with the non-linear or density-dependent couplings [25, 26]. Here we show briefly the one corresponding to the non-linear point coupling (NL-PC) interactions. The starting point of the relativistic NL-PC density functional is the following Lagrangian:

\[ \mathcal{L} = \bar{\psi} \left( i \gamma_{\mu} \partial^\mu - M_\beta \right) \psi - \mathcal{L}_{\text{lin}} - \mathcal{L}_{\text{nl}} - \mathcal{L}_{\text{dec}} - \mathcal{L}_{\text{cou}}, \tag{2} \]

where

\[ \mathcal{L}_{\text{lin}} = \frac{1}{2} \alpha_s \rho_\alpha^2 + \frac{1}{2} \alpha_T \rho_{TS}^2 + \frac{1}{2} \alpha_V \partial V, \]
\[ \mathcal{L}_{\text{nl}} = \frac{1}{3} \beta_s \rho_\alpha^3 + \frac{1}{3} \beta_{TS} \rho_{TS}^3 + \frac{1}{3} \beta_V \partial V, \]
\[ \mathcal{L}_{\text{dec}} = \frac{1}{2} \delta_s \left[ \partial_s \rho_\alpha^2 \right] + \frac{1}{2} \delta_T \left[ \partial_T \rho_{TS}^2 \right] + \frac{1}{2} \delta_V \left[ \partial_V \rho_V^2 \right], \]
\[ \mathcal{L}_{\text{cou}} = \frac{1}{4} F_{\mu \nu} F_{\mu \nu} + e \epsilon_{\alpha \beta \gamma \delta} \partial_\alpha A_\beta \partial_\gamma A_\delta, \tag{3} \]

are the linear, non-linear, and derivative couplings and the Coulomb part, respectively. \( M_\beta \) is the nucleon mass, \( \alpha_s, \alpha_T, \alpha_V, \beta_s, \beta_T, \gamma_\alpha, \delta_s, \delta_T, \delta_V \) and \( \epsilon \) are the electric charge, \( \rho_\alpha, \rho_{TS}, \partial \), and \( \partial_V \) are the isoscalar density, isovector density, iso-scalar current, and iso-vector current, respectively. The densities and currents are defined as:

\[ \rho_\alpha = \bar{\psi} \psi, \tag{4} \]
\[ \rho_{TS} = \bar{\psi} \gamma_\mu \psi, \tag{5} \]
\[ \partial_\alpha = \bar{\psi} \gamma_\mu \gamma_5 \psi, \tag{6} \]
\[ \partial_T = \bar{\psi} \gamma_\mu \gamma_5 \gamma_\tau \psi. \tag{7} \]

Starting from the above Lagrangian, using the Slater determinants as trial wave functions and the Fock term as well as the contributions to the densities and currents from the negative energy levels, one can derive the equations of motion for the nucleons. Moreover, for systems with time reversal symmetry, only the time-like components of the vector currents (6) and (7) survive. The resulted equation for the nucleons reads

\[ \hat{H}_{\psi} = \left( \alpha \cdot p + \beta (M + S (r)) + V (r) \right) \psi = \epsilon \psi, \tag{8} \]

where the potentials \( V (r) \) and \( S (r) \) are calculated as

\[ S = \alpha_s \rho_\alpha + \alpha_T \rho_{TS} + \gamma_\alpha \rho_\alpha^3 + \delta_s \Delta \rho_\alpha + \left( \alpha_T \rho_{TS} + \delta_T \Delta \rho_{TS} \right) \tau_3, \]
\[ V = \alpha_V \rho_V + \gamma_\tau \rho_\tau^3 + \delta_V \Delta \rho_V + \left( \alpha_T \rho_{TV} + \delta_T \Delta \rho_{TV} \right) \tau_3. \tag{9} \]

An axially deformed harmonic oscillator (ADHO) basis is adopted for solving the Dirac equation [25,26,33]. The ADHO basis are defined as the eigen solutions of the Schrodinger equation with an ADHO potential [34,35],

\[ \left[ -\frac{\hbar^2}{2M} \nabla^2 + V_B (z, \rho) \right] \Phi_\alpha (r) = E_\alpha \Phi_\alpha (r), \tag{11} \]

where

\[ V_B (z, \rho) = \frac{1}{2} M \left( \omega_b^2 \rho^2 + \omega_\tau^2 z^2 \right), \tag{12} \]

is the axially deformed HO potential and \( \omega_b \) and \( \omega_\tau \) are the oscillator frequencies along and perpendicular to z axis, respectively. The solution of Eq. (11) reads

\[ \Phi_\alpha (r) = C_\alpha \phi_\alpha (z) R_{\rho,\tau}^n (\rho, \tau), \tag{13} \]

where \( \phi_\alpha (z) \) and \( R_{\rho,\tau}^n (\rho, \tau) \) are the HO wave functions,

\[ \phi_\alpha (z) = \frac{1}{\sqrt{b_z}} \frac{1}{\sqrt{2^n n!}} H_n \left( \frac{z}{b_z} \right) e^{-z^2/2b_z}, \]
\[ R_{\rho,\tau}^n (\rho, \tau) = \frac{1}{b_\rho} \frac{1}{\sqrt{\left( n_\rho + |m| \right)! |m|!}} f_{\rho,\tau}^{|m| \rho} \left( \frac{\rho}{b_\rho} \right) e^{-\rho^2/2b_\rho^2}, \tag{14} \]

\( \chi_\alpha \) is a two component spinor and \( C_\alpha \) is a complex number inserted for convenience. Oscillator lengths \( b_z \) and \( b_\rho \) are related to the frequencies by \( b_z = 1/ \sqrt{M \omega_z} \) and \( b_\rho = 1/ \sqrt{2M \omega_\rho} \).

These basis are also eigen functions of the z component of the angular momentum \( j_z \) with eigen values \( K = |m| + m_z \). For any basis state \( \Phi_\alpha (r) \), the time reversal operator is defined as \( \Phi_\alpha (r) = \mathcal{T} \Phi_\alpha (r) \), where \( \mathcal{T} = ie \sigma_y K \) is the time reversal operator and \( K \) is the complex conjugation. Apparently we have \( K_\alpha = -K_\alpha \) and \( \pi_\alpha = \pi_\alpha \). These basis form a complete set for expanding any two-component spinors.

For a Dirac spinor with four components,

\[ \psi (r) = \left( \sum_\alpha f_\alpha \Phi_\alpha (r) \right) \frac{1}{\sqrt{2\pi}} \exp(\text{i} \text{m} \varphi). \tag{15} \]

The nucleus is assumed to be symmetric under the \( V_4 \) group, that is, for all the potentials and densities we have

\[ f (\rho, \pi \pm \varphi, z) = f (\rho, 2\pi - \varphi, z) = f (\rho, \varphi, z). \tag{17} \]

Thus the components \( f_\alpha \)'s satisfy \( f_\alpha = f_\alpha^* = f_\alpha \) and all the terms with odd \( \text{m} \) vanish. The expansion Eq. (16) can be simplified as

\[ f (\rho, \varphi, z) = f_0 (\rho, \varphi, z) \frac{1}{\sqrt{2\pi}} + \sum_{n=1}^\infty f_n (\rho, \varphi, \frac{1}{\sqrt{2\pi}} \cos(2n\varphi). \tag{18} \]
where
\[ f_0(\rho, z) = \frac{1}{\sqrt{2\pi}} \int_0^{2\pi} d\varphi f(\rho, \varphi, z), \]
\[ f_\alpha(\rho, z) = \frac{1}{\sqrt{\pi}} \int_0^{2\pi} d\varphi f(\rho, \varphi, z) \cos(2n\varphi), \quad (19) \]
are real functions of \( \rho \) and \( z \).

The total energy of a nucleus reads
\[ E_{\text{total}} = \int d^3r \left\{ \sum_k \rho_k^2 \tilde{\psi}_k^\dagger (\alpha \cdot \mathbf{p} + \beta M) \psi_k \right. \]
\[ + \frac{1}{2} \alpha_s \rho_s^2 + \frac{1}{2} \alpha_p \rho_p^2 + \frac{1}{2} \alpha_T \rho_T^2 + \frac{1}{2} \alpha_V \rho_V^2 \]
\[ + \frac{1}{3} \beta_s \rho_s^3 + \frac{1}{4} \gamma_s \rho_s^4 + \frac{1}{4} \gamma_p \rho_p^4 \]
\[ + \frac{1}{2} \delta_s A \rho_s + \frac{1}{2} \delta_p A \rho_p + \frac{1}{2} \delta_V A \rho_V \]
\[ + \frac{1}{2} \beta_s A \rho_s^2 + \frac{1}{2} \gamma_s A \rho_s^3 \]
\[ + \frac{1}{2} \delta_A A \rho_s^2 + \frac{1}{2} \delta_A \rho_s + \frac{1}{2} \rho_c A + E_{\text{pair}} + E_{\text{c.m.}} \right\}, \quad (20) \]
where the center of mass correction \( E_{\text{c.m.}} \) can be calculated either phenomenologically or microscopically.

The intrinsic multipole moments are calculated from the vector densities by
\[ Q_{\lambda \nu} = \int d^3r \rho(\mathbf{r}) \mathbf{r}^\lambda Y_{\lambda \nu}(\Omega), \quad (21) \]
where \( Y_{\lambda \nu}(\Omega) \) is the spherical harmonics and \( \tau \) refers to the proton, neutron or the whole nucleus.

The potential energy surface (PES) is obtained by the constrained self-consistent calculation,
\[ E' = \langle \hat{H} \rangle + \sum_{\mu=1}^{N_c} \frac{1}{2} C_\mu \left( \langle \hat{Q}_\mu \rangle - \mu_0 \right)^2, \quad (22) \]
where \( \hat{H} \) is the RMF Hamiltonian, \( \hat{Q}_\mu \)'s are the multipole operators to be constrained and \( N_c \) is the dimension of the constraining space.

Both the BCS approach and the Bogoliubov transformation are implemented in our model to take into account the pairing effects. For the pairing force, we can use a delta force or a separable finite-range pairing force \([36,37,38]\).

More details of the multi-dimensional constraint covariant density functional theories can be found in Refs. \([25,26]\).

### 3 Results and discussions

#### 3.1 One-, two-, and three-dimensional potential energy surface of \(^{240}\text{Pu}\)

In Ref. \([25]\), one- \((1-d)\), two- \((2-d)\), and three-dimensional \((3-d)\) constrained calculations were performed for the actinide nucleus \(^{240}\text{Pu}\). The parameter set PC-PK1 is used \([39]\).

In Fig. 2 we show the 1-d potential energy curves (PEC) from an oblate shape with \(\beta_{20}\) about \(-0.2\) to the fission configuration with \(\beta_{20}\) beyond 2.0 which are obtained from calculations with different self-consistent symmetries imposed: the axial (AS) or triaxial (TS) symmetries combined with reflection symmetric (RS) or asymmetric cases. The importance of the triaxial deformation on the inner barrier and that of the octupole deformation on the outer barrier are clearly seen: The triaxial deformation reduces the inner barrier height by more than 2 MeV and results in a better agreement with the empirical datum: the RA shape is favored beyond the fission isomer and lowers very much the outer fission barrier. Besides these features, it was found for the first time that the outer barrier is also considerably lowered by about 1 MeV when the triaxial deformation is allowed. In addition, a better reproduction of the empirical barrier height can be seen for the outer barrier. It has been stressed that this feature can only be found when the axial and reflection symmetries are simultaneously broken \([25]\).

In order to see how the PES of \(^{240}\text{Pu}\) becomes unstable against the triaxial distortion, 2-d PES’s from calculations without and with the triaxial deformation were compared in Fig. 3 \([25]\). When the triaxial deformation is allowed, the binding energy of \(^{240}\text{Pu}\) assumes its lowest possible value at each \((\beta_{20}, \beta_{30})\) point. At some points, especially those around the two saddle points, non-axial solutions are favored than the axial ones. The inner barrier height is lowered by about 2 MeV. About 1 MeV is gained for the binding energy at the second saddle point due to the triaxiality. In the regions around the ground state and in the fission isomer valleys, only axially symmetric solutions are obtained.

A full 3-d PES has been obtained for \(^{240}\text{Pu}\) \([25]\). In Fig. 4 are shown only five typical sections of the 3-d PES of \(^{240}\text{Pu}\) in the \((\beta_{22}, \beta_{30})\) plane calculated around the ground state, the first saddle point, the fission isomer, the second saddle point, at a point beyond the outer barrier, respectively. The following conclusions were drawn by examining these 3-d PES’s \([25]\): (1) The ground state and the fission isomer are both axially and reflection symmetric. The stiffness of the fission isomer is much larger than that of the ground state against both the \(\beta_{22}\) and \(\beta_{30}\) distortions.
3.2 Inner and outer fission barriers of even-even actinide nuclei

Guided by the features found in the 1-d, 2-d, and 3-d PES’s of $^{240}$Pu, the fission barrier heights were extracted for even-even actinide nuclei [25]. The calculated values were compared with empirical ones recommended in RIPL-3 [40].

As it has been shown previously, around the inner barrier an actinide nucleus assumes triaxial and reflection symmetric shapes. Thus in order to obtain the inner fission barrier height we can safely make a one-dimensional constraint calculation with the triaxial deformation allowed and the reflection symmetry imposed. In Fig. 5(a) we show the calculated inner barrier heights $B_i^0$ and compare them with the empirical values. It is seen that the triaxiality lowers the inner barrier heights of these actinide nuclei by $1 \sim 4$ MeV as what has been shown in Ref. [13]. In general the agreement of our calculation results with the empirical ones is very good with exceptions in the two thorium isotopes and $^{238}$U. Possible reasons for these disagreements were discussed in Ref. [25].
To obtain the outer fission barrier height \( B_0 \), the situation becomes more complicated because more shape degrees of freedom play important roles around the outer fission barrier. In Ref. [25], 2-d constraint calculations were made carefully around the two saddle points for even-even actinide nuclei. In the lower panel of Fig. 5 we show the results of outer barrier heights \( B_0 \) and compare them with empirical values. For most of the nuclei investigated here, the triaxiality lowers the outer barrier by \( 0.5 \sim 1 \) MeV, accounting for about \( 10 \sim 20\% \) of the barrier height.

One finds that the calculation with the triaxiality agrees well with the empirical values and the only exception is \( 248 \)Cm. From the calculation with the axial symmetry imposed, the outer barrier height of \( 248 \)Cm is already smaller than the empirical value. The reason for this discrepancy may be related to that there are two possible fission paths beyond the first barrier [25].

In Ref. [25], it was also examined the parameter dependency of the influence of triaxiality on the outer fission barrier and the lowering effect of the triaxiality on the outer fission barrier was also observed when parameter sets other than PC-PK1 are used.

### 3.3 Non-axial octupole shapes in \( N = 150 \) isotones

Nowadays the study of nuclei with \( Z \sim 100 \) becomes more and more important because it not only reveals the structure of these nuclei themselves but also provides significant information for superheavy nuclei [41,42,43,44]. One of the relevant and interesting topics is how to explain the low-lying \( 2^- \) states in some \( N = 150 \) even-even nuclei. In these nuclei, the bandhead energy \( E(2^-) \) of the lowest \( 2^- \) bands is very low [45]. It is well accepted that the octupole correlation is responsible for it. For example, a quasiparticle phonon model with octupole correlations included was used to explain the excitation energy of the \( 2^- \) state of the isotones with \( N = 150 \) [46]. In Ref. [47], Chen et al. proposed that the non-axial octupole \( Y_{32} \)-correlation results in the experimentally observed low-energy \( 2^- \) bands in the \( N = 150 \) isotones and the reflection asymmetric shell model calculations reproduces well the experimental observables of these \( 2^- \) bands.

The non-axial reflection-asymmetric \( \beta_{32} \) shape in some transmerium nuclei with \( N = 150 \), namely \( 246 \)Cm, \( 248 \)Cf, \( 250 \)Fm, and \( 252 \)No were investigated with the multidimensional constrained covariant density functional theory [48]. The parameter set DD-PC1 is used [49]. For the ground states of \( 248 \)Cf and \( 250 \)Fm, the non-axial octupole deformation parameter \( \beta_{32} > 0.03 \) and the energy gain due to the \( \beta_{32} \) distortion is larger than \( 300 \) keV. In \( 246 \)Cm and \( 252 \)No, shallow \( \beta_{32} \) minima are found.

The triaxial octupole \( Y_{32} \) effects stem from the coupling between pairs of single-particle orbits with \( \Lambda j = \Lambda l = 3 \) and \( \Delta K = 2 \) where \( j \) and \( l \) are the total and orbit angular momenta of single particles respectively and \( K \) the projection of \( n \) on the \( z \) axis. In Fig. 6, we show the proton and neutron single-particle levels near the Fermi surface for \( 248 \)Cf as a function of \( \beta_{32} \) with \( \beta_{20} \) fixed at 0.3. It was shown that the spherical proton orbitals \( n2f_{7/2} \) and \( n1i_{13/2} \) are very close to each other [48]. This near degeneracy results in octupole correlations. As seen in Fig. 6, the two proton levels, \([521]3/2 \) originating from \( 2f_{7/2} \) and \([633]7/2 \) originating from \( 1i_{13/2} \), are very close to each other and just lie above and below the Fermi surface. This leads to the development of a gap at \( N = 150 \) with \( \beta_{32} \) increasing. The \( Y_{32} \) correlation in \( N = 150 \) isotones is from both the proton and the neutron and for \( 248 \)Cf is the correlation is the most pronounced [48].

### 4 Summary

In this contribution we present some applications of the multi-dimensional constrained covariant density functional...
theories in which all shape degrees of freedom $\beta_{l\nu}$ deformations with even $\mu$ are allowed. The potential energy surfaces of actinide nuclei in the $(\beta_{20}, \beta_{22}, \beta_{30})$ deformation space are investigated. It is found that besides the octupole deformation, the triaxiality also plays an important role upon the second fission barriers. For most of even-even actinide nuclei, the triaxiality lowers the outer barrier by 0.5 $\pm$ 1 MeV, accounting for about 10 $\sim$ 20% of the barrier height. The non-axial reflection-asymmetric $\beta_{32}$ shape in some transformium nuclei with $N = 150$, namely 246Cm, 248Cf, 250Fm, and 252No are studied. Due to the interaction between a pair of neutron orbitons, [734][9/2 originating from $v_{F15/2}$ and [622]5/2 originating from $v_{F9/2}$, and that of a pair of proton orbitons, $[521]3/2$ originating from $\pi_f1/2$ and [633]7/2 originating from $\pi_{13/2}$, rather strong non-axial octupole $\gamma_{32}$ effects have been found for 248Cf and 250Fm which are both well deformed with large axial-quadrupole deformations, $\beta_{32} \approx 0.3$. For 246Cm and 252No, a shallow minima develops along the $\beta_{32}$ deformation degree of freedom.

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