Magnetospheric Accretion and Winds on the T Tauri Star SU Aurigae: Multi-Spectral Line Variability and Cross-Correlation Analysis.*

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Abstract. SU Aurigae is a T Tauri star that was well monitored during the MUSICOS 96 multi-site campaign. We present the results of the spectroscopic analysis of the circumstellar environment of this star, particularly of the Hα, Hβ, NaI D and HeI D3 line profiles. The signatures of modulated outflows and mass accretion events are analysed, as well as transient spectral features. We compute the cross-correlation function (CCF) of several pairs of (velocity bins in) spectral lines to better investigate the profiles’ temporal variability. We found increasing time lags between the variability of HeI D3, NaI D and Hβ. We propose this may be understood in terms of azimuthal distortion of the magnetic field lines due to the different rotation rates of the star and the disk. We find the slightly blueshifted absorption features in Hα, Hβ and NaI D to be anti-correlated with the accretion flow signatures. We propose that the transient absorption features in the blue wings of Hα, Hβ and NaI D (signatures of mass outflows), and flare brightenings are related to the disruption of distorted magnetospheric field lines.

Key words: Stars: pre-main sequence – Circumstellar matter – Line: profiles – Stars: activity – Stars: magnetic fields – Stars: individual: SU Aur

1. Introduction

1.1. Classical T Tauri Stars

T Tauri stars (TTS) are low-mass (M < 3 M⊙) pre-main sequence stars which are normally younger than 3 × 10⁶ years (Appenzeller & Mundt 1989). They are of great interest as prototypes of young solar-type stars. Historically two sub-groups of TTS were defined, based on the strength of the Hα spectral line emission: classical T Tauri stars (CTTS) with strong Hα emission and weak (or “naked”) T Tauri stars (WTTS). The enhanced activity of most CTTS as seen from the Balmer and metallic (permitted and forbidden) line emission is believed to be due to the presence of an accretion disk, whose UV and IR excess emission causes also broad energy distributions.

Since the first studies of their line profiles it has been known that CTTS spectra show evidence of outflows (e.g. Herbig 1962). More recently also abundant observational evidence of funnel accretion flows onto CTTS has been published (e.g. Edwards et al. 1994).

Königl (1991) proposed the application of the Ghosh & Lamb (1978) magnetospheric model, developed for accreting neutron stars, to explain the interaction between CTTS and their accretion disk. The accretion disk is disrupted at a few stellar radii from the central star (close to the co-rotation radius) by the presence of a stellar dipole magnetic field. According to Shu et al. (1994) and Paatz & Camenzind (1996), at the truncation point, the ionized disk material is loaded either onto inner closed magnetic field lines, accreting thereby onto the stellar surface, or it is loaded onto outer open magnetic field lines that can drive a disk-wind flow.

Recently, some observational support for the magnetospheric models was presented by Johns-Krull et al. (1999).
and Guenther et al. (1999), who measured kilogauss magnetic fields at the surface of CTTS, enough to effectively disrupt the accretion disk at a few stellar radii. The assumption of a stellar dipole magnetic field aligned with the rotation axis completely determines the geometry and dynamics of the disk-star interaction. According to the magnetospheric models mentioned previously, the magnetosphere is axi-symmetric with respect to the rotational axis so no rotational modulation is expected in the wind and accretion signatures, unless the disk is inhomogeneous at the truncation radius. Furthermore, variations in the inflow and outflow signatures should be approximately in phase. But a stellar magnetic field that has solely a dipolar component is unlikely and this type of models has been criticised (Safler 1998; Alencar & Basri 2000). The evidence for magnetospheric accretion exists (hot spots and redshifted absorption features), but theoretical models are still far from explaining the variety of observations.

1.2. SU Aurigae

SU Aurigae has been classified as a CTTS (e.g. Bouvier et al. 1993), but also as the prototype of a separate class of T Tauri stars, the SU Aur type stars (Herbig & Bell 1988). SU Aur has a G2 spectral type (Herbig 1960), thus, due to the contrast with a hotter photosphere, only Hα, and occasionally Hβ, appear in emission in the spectrum. SU Aur has an exceptionally high projected rotational velocity of 60 km s⁻¹ (Johns-Krull 1996; Unruh et al. 2000) and a rotational period of about 3 days. Photometric period measurements for SU Aur are very difficult to make. For instance, Bouvier et al. (1993) found multiple periods, with 2.78 days the most likely period. So far the best period estimates come from the analysis of the spectral variations of the Balmer lines. Giampapa et al. (1993) found a period of 2.98 ± 0.4 days in the blue wing of the Hα line, later confirmed also in the blue and red wings of Hβ by Johns & Basri (1995). Petrov et al. (1996) reported a period of 3.03 ± 0.003 days measured on the red wings of the Balmer lines. Our data set suggests a shorter rotational period of about 2.6 to 2.8 days (Unruh et al. 2000).

1.3. Diagnostics and Models of Magnetospheric Accretion

From period analysis and equivalent width measurements of fitted components in Hα and Hβ, Johns & Basri (1995) observed that the Hβ redshifted absorption feature and the Hα blueshifted absorption feature (respectively accretion and wind signatures) show a periodicity of about 3 days and are approximately 180° out of phase in SU Aur. This led them to propose a generalization of the magnetospheric model, in which the rotational axis and the magnetic dipole axis are (slightly) misaligned: the misaligned “egg-beater” or oblique rotator model. It predicts that the signatures of mass accretion and disk winds should be rotationally modulated and approximately in anti-phase, as they observed in SU Aur.

Using Hα, Hβ, Na i D and He i D3, we try to disentangle the two main contributions present in the line profiles, namely accretion and wind signatures. These lines probe different parts of the circumstellar environment. Thus, the temporal relation between the variability in the different lines depends on the geometry and physical conditions of the circumstellar environment, in particular of the inner disk and magnetosphere. For instance, variations in the accretion rate at the inner disk or outer magnetosphere will first affect low excitation energy features arising in this region. The higher energy lines that form in the inner accretion stream or in the accretion shock will be affected by this “perturbation” after a time lag related to the infall time through the magnetosphere. This delay is expected to be of the order of several hours (Smith et al. 1997).

Previous SU Aur data sets typically had one to two spectra a night, even though over long time spans. Our data set, with finer time sampling, allows us for the first time to study the variations of the different components in spectral lines on short timescales. In the context of the magnetospheric model and using cross-correlation techniques, we have searched for time lags between the variability of the mentioned spectral lines. In Sect. 3 we describe the implementation and results of the cross-correlation analysis of our data set. In Sect. 4 we present our interpretations in the frame of accretion and wind processes. In Sect. 5 we describe two transient absorption features observed in Hα, Hβ and Na i D and we analyse their velocity evolution.

2. Description of the SU Aur Data Set

2.1. MUSICOS 96 Campaign

The MUSICOS (MUlti-SIte COntinuous Spectroscopy) network was created to provide continuous spectroscopic coverage for stellar objects, whose variability timescales demand simultaneous coverage from several longitudes (Catala & Foing 1990, Catala et al. 1993, Catala & Foing 1994). To fulfill this aim, existing observational capabilities were used or dedicated instruments were developed. A MUSICOS campaign is organized every two years and several stellar targets are selected for each campaign.

Our data set was obtained in November 1996 during the MUSICOS 96 multi-wavelength campaign, that involved five different observatories: Isaac Newton Telescope (INT, La Palma), Observatoire de Haute Provence (OHP, France), McDonald Observatory (MDO, USA), Beijing Astronomical Observatory (BAO, Xinglong, China) and Canada-France-Hawaii Telescope (CFHT, Hawaii). We obtained 126 echelle spectra of SU Aur, spanning 10.5 days, with 3.5 days covered almost continuously. Hα, Na i D and He i D3 were observed at all five observatories while Hβ could only be observed from the INT, OHP and CFHT. Thus, for this line, we obtained only 72 spectra. The data from the different observatories were re-
binned to a uniform resolution of 30,000, or approximately 10 km s$^{-1}$. The journals of the observations and more details about this campaign and data reduction can be found in Unruh et al. (2000).

2.2. Brief Summary of Variability in the Data Set

![Fig. 1. The average (line plots) and variance (shaded plots) of (a) H$\alpha$, (b) H$\beta$, (c) Na\textsc{i} D and (d) He\textsc{i} D3. The y-axis scale on the left is for the average and on the right for the variance. For H$\alpha$ and H$\beta$, a rotationally broadened template profile is plotted (dot-dashed line in (a) and (b)) as a photospheric reference. The narrow feature that appears in the variance profiles of H$\alpha$, H$\beta$, Na\textsc{i} D, and He\textsc{i} D3, is the signature of transient outflows (Sect. 5). The sharply peaked central feature visible in the variance profile of Na\textsc{i} D is related to the narrow interstellar component. The two components present in the He\textsc{i} D3 profile are also plotted (dot-dashed line in (d)); the smaller features appearing at 180 and 230 km s$^{-1}$ are telluric water residues. The vertical dotted lines appearing in all the graphs are the velocity bins chosen for the CCF analysis (Sect. 3.2); the bin size is 5 km s$^{-1}$.](image)

We highlight in this subsection the main characteristics of the variability in our data set. The period analysis was performed by Unruh et al. (1998, 2000). They computed the periodograms of the above mentioned spectral lines (see figures in Unruh et al. 2000). We independently determined the following periods: 2.63 days in He\textsc{i} D3 [−75:175] km s$^{-1}$ and in the red wings of Na\textsc{i} D [30:150] km s$^{-1}$, and 2.80 days in the red wing of H$\beta$ [50:175] km s$^{-1}$ and in the far blue wing of H$\alpha$ [−375:−175] km s$^{-1}$. This might indicate that the regions of formation of these lines are not strictly in co-rotation. However, the peaks in the periodograms are fairly broad, thus these periods are all consistent with a single periodicity, between 2.5 and 3 days.

In the periodogram of H$\alpha$, and less conspicuously in the periodograms of H$\beta$ and Na\textsc{i} D, there is a broad peak at about 5 days that we believe to be related to the flux enhancement observed in H$\alpha$ and H$\beta$ at roughly the middle of the time series (Sect. 3.2). We have computed the periodograms of the spectral lines, removing the spectra affected by this flux enhancement. We confirm our period determinations and, in fact, the peak at 5 days vanishes.

In Fig. 1 we show the average and variance profiles of H$\alpha$, H$\beta$, Na\textsc{i} D and He\textsc{i} D3. We also plot a rotationally broadened photospheric template for the two Balmer lines to indicate clearly the circumstellar contribution (Fig. 1a, b). In both Balmer lines and in Na\textsc{i} D transient outflows are present. These appear in the variance profiles of these lines as the peaks between −150 and −50 km s$^{-1}$. Small mismatches in the wavelength calibration between the different sites and the rebinning of the data cause the narrow features in the Na\textsc{i} D variance profile at the position of the interstellar absorption lines.

The average profile of He\textsc{i} D3 is very asymmetric and appears to be formed by two components, one at rest velocity and a redshifted component (Fig. 1d). The rest component is obtained, in a crude decomposition, by reflecting the blue wing of the average profile about zero velocity. The redshifted component is isolated by subtracting this reflection from the average profile. This component is centered at approximately 83 km s$^{-1}$. The two components are broader than 2 × v sin i and the redshifted component extends at least until 200 km s$^{-1}$.

3. Multi-Line Cross-Correlation Analysis

The spectrum of SU Aur is rich in spectral lines thought to originate from the circumstellar environment of the star. The Balmer lines, H$\alpha$ and H$\beta$, the Na\textsc{i} D and He\textsc{i} D3 lines, due to their different physical properties, probe different parts of the circumstellar material. Furthermore, in these lines mingle several different components: Giampapa et al. (1993) and Johns & Basri (1995b) proposed that the profiles of, respectively, H$\alpha$ and H$\beta$ could be decomposed in the contributions of an enhanced chromosphere, and a slow and a fast wind components.

The total time span of our data set allows us to sample variability related to rotational modulation. With our fine time sampling, we also expect to characterize variability on much shorter time scales, for instance arising from the inner magnetosphere. We intend to analyse how variability propagates through the different spectral lines. In our analysis of these complex profiles, we chose the cross-correlation function that expresses how the correlation coefficient between two time series varies with the
Cross-correlation techniques have been widely used in variability studies of active galactic nuclei (White & Peterson 1994). Smith et al. (1999) applied this method to the equivalent width of the Balmer and Ca II H & K lines for several T Tauri stars, including SU Aur, but their low-resolution spectra did not allow to disentangle the different components that mingle in those spectral lines. This technique was also previously used, for instance, in Johns & Basri (1995a) for the analysis of Hα in several CTTS (also SU Aur) and Johns-Krull & Basri (1997) for the analysis of several lines in another TTS DF Tau.

We calculated the cross-correlation function (CCF) of pairs of spectral lines as a function of the time lag $\tau$ as well
as the auto-correlation functions (ACF). In Appendix A we define the CCF and describe its implementation for our type of time series, as well as the error analysis.

3.1. Application of CCF Analysis to SU Aur Data

Using the technique described in Appendix A, we computed for each pair of spectral lines a cross-correlation function intensity map that allows a first glimpse at the time lag information contained in the time series. These maps were calculated for each pair of spectral lines for lags multiple of 0.25 days (6 h). In Fig. 2 we present the most striking examples of the results we obtained. Each column in this figure represents the CCF computed at three representative time lags: 0, \( \sim P/2 \) and \( \sim P \), where \( P \) is the rotational period, taken to be approximately 2.75 days. It can be seen that the periodicity in the spectral lines is reflected in the behaviour of the CCFs with time lag. The CCFs vary from high positive correlation coefficient to high negative correlation coefficient in a periodic way (e.g. Fig. 2b). These maps illustrate the time relation between the different spectral lines (Oliveira et al. 2000a). The red wing of H\( \beta \) seems to vary approximately in phase with the red wings of H\( \alpha \) and Na\( \text{i} \) D (Fig. 2b,c respectively), and with the whole He\( \text{i} \) D3 profile (Fig. 2a). Furthermore, the blue and red wings of H\( \beta \) seem out of phase (Fig. 2a).

These kind of maps cannot be used to determine time lags with enough precision. Their computation is too time consuming to be a viable tool for a finer analysis with better time sampling. Therefore we have decided to choose and isolate velocity bins in the spectral lines that are representative of the profiles’ variations.

3.2. Velocity Bins for the CCF

We selected coherent velocity domains by analysing the ACF for each spectral line. This is very well illustrated in Fig. 3a for H\( \beta \). In this ACF, we can see that the H\( \beta \) profile is composed of three distinct domains: \([-300: -125]\) km s\(^{-1}\), \([-125: 25]\) km s\(^{-1}\) and \([25: 250]\) km s\(^{-1}\). Within these velocity domains the profile behaves in a concerted way. In each such interval we selected a representative velocity bin for more detailed CCF analysis: \(-150\) km s\(^{-1}\) (the far blue wing), \(-50\) km s\(^{-1}\) (the slightly blueshifted absorption component) and 100 km s\(^{-1}\) (the redshifted absorption component). For H\( \alpha \) three domains are also defined: \([-400: -125]\) km s\(^{-1}\), \([-125: 25]\) km s\(^{-1}\) and \([25: 250]\) km s\(^{-1}\); the appropriate bins are then \(-200\) km s\(^{-1}\), \(-75\) km s\(^{-1}\) and 100 km s\(^{-1}\), corresponding to the same regions in H\( \beta \). For Na\( \text{i} \) D the blue and red wings seem to vary independently; we have thus chosen two velocity bins: \(-30\) km s\(^{-1}\) and 75 km s\(^{-1}\). The profile of He\( \text{i} \) D3 varies as a whole within the interval \([-75: 150]\) km s\(^{-1}\). Still, the He\( \text{i} \) D3 profile seems composed of two components (Sect. 2.2). Thus, we will investigate their behaviour separately, selecting bins at 0 and 83 km s\(^{-1}\). The selected bins for these spectral lines are shown in Fig. 1. In Fig. 3 we plot the intensity variations of the velocity bins that we have selected for each line: from top to bottom, H\( \alpha \), H\( \beta \), Na\( \text{i} \) D1 and He\( \text{i} \) D3.

The H\( \alpha \) intensity variations clearly show the flux enhancement seen both in the blue and red wings of the profile. The enhancement lasted for a minimum of 2 days, and the peak intensity occurs at about \( t = 9 \) days. The increase was \( \sim 65\% \) in the blue wing and \( \sim 72\% \) in the red wing. The central absorption feature (\(-75\) km s\(^{-1}\)) shows, from \( t \sim 12 \) onwards, the presence of the second transient features (see Sect. 5). In the H\( \alpha \) flux variations there are hardly any visible traces of the \( \sim 3 \) day periodicity.

The analysis of the flux enhancement in H\( \beta \) is more complicated as there are fewer data points. Still, the flux enhancement can also be seen, causing variations of
In the red wing of \( H\beta \) with the variations in the rest of the profile. The variations of the far blue wing of \( H\beta \) phase behaviour of these two parts of the \( H\beta \) spectrum show no re-

\( \sim 22 \% \) in the far blue wing and \( \sim 37 \% \) in the red wing. In the red wing of \( H\beta \), the \( \sim 3 \) day periodicity can be seen and in the slightly blueshifted absorption feature there are some indications of this too. Furthermore, the quasi anti-phase behaviour of these two parts of the \( H\beta \) profile can be observed. The variations of the far blue wing of \( H\beta \), with the exception of the flux enhancement, show no relation with the variations in the rest of the profile.

Both components of \( \text{He} \text{I} \) D3 and the red wing of \( \text{Na} \text{I} \) D1, show clear 2.63 days periodicity. The variations are not sinusoidal but the periodic deepening of the absorption features is clear. The behaviour of the blue and red wings of \( \text{Na} \text{I} \) D1 seems anti-correlated.

In order to clarify and compare more easily the variability of the four velocity bins where signatures of periodicity were seen, we folded in time the intensity variations of \( H\beta \) at 100 km s\(^{-1}\), \( \text{Na} \text{I} \) D1 at 75 km s\(^{-1}\) and \( \text{He} \text{I} \) D3 at 83 and 0 km s\(^{-1}\). The intensity variations are plotted against: • time, ◦ (time – \( P \)), * (time – 2\( \times \)P). The period used was \( P = 2.63 \) days. Obviously, the variability of \( H\beta \) has other non-periodic components. Folded in this way, the flux variations in \( \text{He} \text{I} \) D and \( \text{Na} \text{I} \) D clearly show their periodicity. The lagged behaviour of the variations of the three spectral lines is evident.

\(~ 22 \% \) in the far blue wing and \( \sim 37 \% \) in the red wing. In the red wing of \( H\beta \), there is also some non-periodic variability. The behaviour of the other two lines is mainly controlled by the phenomenon with periodicity of \( \sim 2.63 \) days. Very interesting in Fig. 3 is that it makes clearly visible the time-lagged behaviour between the variability of \( \text{He} \text{I} \) D3 at 0 and 83 km s\(^{-1}\), \( \text{Na} \text{I} \) D1 at 75 km s\(^{-1}\) and \( H\beta \) at 100 km s\(^{-1}\). In the remainder of this section we calculate these time lags and relate them to accretion and wind flows.

### 3.3. Time Lags between Multi-Line Variations

We compute the CCF for each pair of chosen velocity bins with a sampling \( \Delta \tau = 0.025 \) day (approximately half of the maximum exposure time) for time lags ranging from \(-4 \) to 4 days (for larger time lags the number of points in the calculation would be too small). For each lag \( \tau \) the CCF is computed with a different number of pairs of points, so the statistical significance of a given value of the correlation coefficient varies with the lag. In our analysis of the CCFs we will consider only peaks significant at more than the 99 % level. We have computed the false alarm probability following Bevington & Robinson (1992).

In Fig. 5 we show some of the CCFs for the pairs of velocity bins that give the most interesting results. In each plot, the CCF is represented with error bars that are obtained from the standard deviation of the Monte Carlo simulations. The periodicity of the CCFs is evident and is a consequence of the periodic variations in the spectral lines analysed. Taking for example Fig. 5f, there is a central peak of the CCF at about \( \tau = 0 \), and two more peaks respectively at \( \pm \) P. For velocity bins where only a weak peak was detected in the period analysis, e.g. the blue wing of \( H\beta \) and the red wing of \( H\alpha \), that is reflected in the amplitude (i.e. correlation coefficient) and shape of their CCFs with respect to the red wing of \( H\beta \) (Fig. 5b,c). On the contrary, the CCFs between clearly periodic time series show sharp peaks with high correlation coefficient, as it is seen for the CCF between the redshifted component of \( \text{He} \text{I} \) D3 and the red wing of \( H\beta \) (Fig. 5e).

The shape of the CCFs could be interpreted as meaning that there are features which appear around a limb of the star, last coherently for half a rotation and then disappear around the other limb. The fact that the “peaks” and “valleys” have similar amplitude could indicate that features on both sides of the star behave similarly. The exception is the case of the two \( \text{He} \text{I} \) D3 components (Fig. 5f).

In Table 1 we list the relevant time lags found for each pair of velocity bins (only the peak closer to zero was analysed in detail). Pairs of velocity bins that did not yield significant lag information or were redundant were discarded. We give both the peak and amplitude of the CCF, the median of the cross-correlation peak distribution (CCPD) and the intervals \( \tau \pm \Delta \tau_{0.7} \), obtained by interpolation of the CCPD (Appendix A). Also listed is the peak’s signifi-
Fig. 5. Cross-correlation as a function of time lag. In each graph the CCF of a pair of selected velocity bins is plotted with the error bars obtained from the Monte Carlo simulations; the spectral lines and the velocity bins used are indicated. The CCFs were calculated with a sampling of $\Delta \tau = 0.025$ day. The recurrence of the peaks is a clear result of the periodicity present in the spectral lines. The amplitude and shape of the CCF reflect how strong was the periodicity detected in the velocity bins.

In this table there are positive and negative lags. This is a matter of convention in the way the CCF is computed. In our case if $CCF(l_1, l_2)$ yields a lag $\tau > 0$ this means that $l_2$ is $\tau$ in advance of $l_1$; conversely if $CCF(l_3, l_2)$ yields a lag $\tau < 0$ it means that $l_3$ is $|\tau|$ in advance of $l_2$. This is relevant when several (velocity bins of) different lines are compared and sorted in time.

The far blue and red wings of $\text{H}_\alpha$ (respectively $-200$ and $100$ km s$^{-1}$) correlate well, with a single broad peak at approximately zero lag. Also well correlated at zero lag with these $\text{H}_\alpha$ regions is the far blue wing of $\text{H}\beta$. 

Table 1. Time lags found for several pairs of velocity bins. Pairs that do not yield significant lags or provide redundant information are not listed. \( CCF(l_1,l_2) \) is the cross-correlation function of \( l_1 \) and \( l_2 \). In the first four columns, the spectral lines and velocity bins are given. The peak and amplitude of the \( CCF \) are listed in columns 5 and 6, the median (\( \bar{\tau} \)) and \( \bar{\tau} + \Delta \tau \) of the cross-correlation probability distribution in columns 7, 8 and 9. The statistical significance of the peak by means of the false alarm probability (FAP) is given in the last column. The first six \( CCFs \) are listed in the order as they appear in Fig. 4.

| line 1 (\( \text{km s}^{-1} \)) | line 2 (\( \text{km s}^{-1} \)) | peak (\( \text{days} \)) | amplitude | \( \bar{\tau} - \Delta \tau \) (\( \text{days} \)) | \( \bar{\tau} + \Delta \tau \) (\( \text{days} \)) | FAP peak |
|-----------------|-----------------|--------------|-----------|----------------|----------------|---------|
| H\( \beta \) 50 | H\( \beta \) 100 | 0.075 0.62 | 1.670 1.634 | 1.762 | 2 \times 10^{-5} | 4 \times 10^{-7} |
| H\( \alpha \) 200 | H\( \beta \) 100 | 0.550 0.63 | 0.525 0.422 | 0.544 | 5 \times 10^{-5} | 3 \times 10^{-7} |
| H\( \alpha \) 100 | H\( \beta \) 100 | 0.275 0.55 | 0.272 0.192 | 0.406 | 3 \times 10^{-5} | 3 \times 10^{-9} |
| Na\( \alpha \) 75 | H\( \beta \) 100 | -0.175 0.64 | -0.188 -0.288 | -0.095 | 5 \times 10^{-5} | 2 \times 10^{-16} |
| He\( \alpha \) 30 | H\( \beta \) 100 | -0.275 0.72 | -0.273 -0.356 | -0.027 | 2 \times 10^{-16} | 2 \times 10^{-3} |
| He\( \alpha \) 0 | Na\( \alpha \) 80 | -0.125 0.69 | -0.130 -0.162 | -0.071 | 3 \times 10^{-3} | 4 \times 10^{-14} |
| He\( \alpha \) 80 | H\( \beta \) -150 | -0.650 0.47 | -0.725 -0.967 | -0.580 | 3 \times 10^{-3} | 5 \times 10^{-14} |
| He\( \alpha \) 80 | H\( \beta \) -50 | -1.750 0.51 | -1.770 -1.843 | -1.341 | 1 \times 10^{-3} | 1 \times 10^{-18} |
| He\( \alpha \) 80 | H\( \alpha \) -200 | -0.650 0.52 | -0.710 -0.861 | -0.619 | 2 \times 10^{-3} | 1 \times 10^{-11} |
| He\( \alpha \) 80 | H\( \alpha \) -75 | -1.900 0.38 | -1.906 -1.946 | -1.203 | 2 \times 10^{-3} | 1 \times 10^{-11} |
| He\( \alpha \) 80 | Na\( \alpha \) 100 | -0.650 0.34 | -0.620 -0.670 | -0.516 | 4 \times 10^{-3} | 4 \times 10^{-14} |
| He\( \alpha \) 0 | Na\( \alpha \) 75 | -0.075 0.65 | -0.079 -0.097 | -0.058 | 4 \times 10^{-3} | 4 \times 10^{-14} |
| He\( \alpha \) 80 | Na\( \alpha \) -30 | -2.050 0.40 | -1.883 -2.097 | -1.722 | 2 \times 10^{-3} | 1 \times 10^{-18} |
| He\( \alpha \) 80 | Na\( \alpha \) 75 | -0.050 0.72 | -0.038 0.026 | -0.058 | 1 \times 10^{-18} | 1 \times 10^{-18} |
| H\( \alpha \) -75 | H\( \beta \) -50 | -0.125 0.76 | -0.130 -0.254 | -0.047 | 1 \times 10^{-18} | 1 \times 10^{-18} |
| H\( \alpha \) -200 | H\( \alpha \) 100 | -0.075 0.88 | -0.087 -0.096 | -0.079 | 1 \times 10^{-18} | 1 \times 10^{-18} |
| H\( \alpha \) -200 | H\( \beta \) -150 | -0.075 0.76 | -0.084 -0.110 | -0.052 | 1 \times 10^{-18} | 1 \times 10^{-18} |

\((-150 \text{ km s}^{-1})\). This is probably due to the contribution of a turbulent broadening mechanism (e.g. Basri 1990; Edwards et al. 1994; Alencar & Basri 2003). The peak of the \( CCF \) between the red wings of the two Balmer lines is at approximately 0.3 days (Fig. 4c), indicating a delay between the variability effect on the two lines. The \( CCF \) of the blueshifted absorption feature in H\( \alpha \) \((-75 \text{ km s}^{-1})\), and the equivalent feature in H\( \beta \) \((-50 \text{ km s}^{-1})\), shows a very broad peak at approximately lag \( \tau = 0 \). As a whole, the H\( \alpha \) profile correlates less well than H\( \beta \) with the other lines. This is because the different effects mingle more in H\( \alpha \) as it originates in a larger volume. The blue and red absorption features in H\( \beta \) \((-50 \text{ and } 100 \text{ km s}^{-1}\) respectively) are anti-correlated at lag \( \tau = 0 \), and show two peaks at lag \( \tau = \pm 0.075 \) (Fig. 4a).

The red absorption features of Na\( \alpha \) D correlate well with the red absorption feature in H\( \beta \) (Fig. 4d) and less well with the red wing of H\( \alpha \). The blue absorption wings of Na\( \alpha \) D are well correlated with the slightly blueshifted absorption features in the Balmer lines. At approximately zero lag, the blueshifted regions of these spectral lines are anti-correlated with the red wings of the same lines.

There seems to be a small lag between the variability that affects the two He\( \alpha \) D3 components, respectively 0 and 80 km s\(^{-1}\) (Fig. 4f). In agreement with this, the \( CCFs \) of the redshifted absorption features in Na\( \alpha \) D and the two He\( \alpha \) D3 components also show slightly different peaks. However, the other spectral lines, when correlated with the He\( \alpha \) D3 components, yield peaks of the \( CCF \) that are consistent with a single time lag. Therefore, in Table 1 we have only listed the \( CCF \) information on one of the He\( \alpha \) D3 components, the component at 80 km s\(^{-1}\).

We believe that the time lag detected between the two He\( \alpha \) D3 components is real but small, thus not always detectable. Both He\( \alpha \) D3 components are well correlated with the red wing of H\( \beta \) (Fig. 4e) and Na\( \alpha \) D. The slightly blueshifted absorption features in H\( \alpha \), H\( \beta \) and Na\( \alpha \) D are anti-correlated at lag \( \tau = 0 \) with He\( \alpha \) D3 and their \( CCF \) shows then two peaks at lag \( \tau = \pm 0.075 \) (Table 1).

Between the redshifted absorption component in Na\( \alpha \) D and the rest absorption component of He\( \alpha \) D a time lag of \(-0.075 \text{ days} \) was found, indicating the advance of the variability in this He\( \alpha \) D3 component. On the other hand, the variability in the redshifted Na\( \alpha \) D component seems to anticipate the variability in the redshifted absorption component in He\( \alpha \) D3 by 0.050 days. This time lag is at the limit of our time resolution, so we believe the variability in these components to be practically simultaneous. The variability of the redshifted absorption component of H\( \beta \) is delayed by about 0.28 days with respect to the variability in the redshifted He\( \alpha \) D3 component.

In summary, the absorption features in the red wings of H\( \beta \) and Na\( \alpha \) D and the He\( \alpha \) D3 line correlate strongly over a large velocity range. The correlation with the red wing of H\( \alpha \) is less clear. Anti-correlated with the red wings of H\( \beta \) and Na\( \alpha \) D, and with He\( \alpha \) D3, are the absorption features in the near blue wings of H\( \alpha \), H\( \beta \) and Na\( \alpha \) D. The far blue (emission) wings of both Balmer lines are well
correlated with each other. We found increasing time lags between the rest absorption component of He\textsc{i} D3, the redshifted absorption components of Na\textsc{i} D and He\textsc{i} D3 and the redshifted H\textbeta absorption component.

4. Interpretation: Accretion, Winds and Disk

4.1. Multi-line Time Lags in SU Aur

Normally, in stars of spectral type G2 there is no He\textsc{i} D3 line. The conditions for the formation of the He\textsc{i} D3 line (high temperature or density) are consistent with this line being formed at the footpoints of the accretion column or slightly above the photosphere, where the kinetic energy is released, or by XUV back-warming of the surface by an active corona. For most CTTS the He\textsc{i} D3 line appears in emission but in SU Aur this line is in absorption. We decompose the He\textsc{i} D3 average profile in two components (Fig. 1d). The component centered at rest velocity probably originates in post-shock gas at the base of the accretion column, and the redshifted component in the accretion column (Najita et al. 2000). We have some indication that there is a time-lagged behaviour between the two components, and this would also be consistent with the two lines being formed in slightly displaced regions. But, the fact that we observe the same period (2.63 days) and that they vary almost in synchrony confirms that the formation of both components is closely linked.

The absorption component in the red wings of Na\textsc{i} D and the He\textsc{i} D3 line vary in an almost synchronized way, implying that the Na\textsc{i} D lines are also formed close to the star. There is a small delay in the variability observed in He\textsc{i} D3 and the variability observed in the absorption component in the red wing of H\textbeta. Magneto-spheric models (e.g. Hartmann et al. 1994) strongly suggest that the redshifted absorption features in the Balmer and metallic lines in CTTSs are formed in the accretion funnels. We conclude then that the Na\textsc{i} D and H\textbeta redshifted absorption features appear to arise in the inner accretion flow, with H\textbeta forming furthest away from the star. In H\alpha the situation is more ambiguous as there is a large bulk emission whose origin is uncertain. Still, the redshifted absorption component in H\alpha is probably also related with the accretion flow, but at larger distances from the star, and the time lags we observe are consistent with this.

The time lags we determined suggest that a perturbation is seen in sucession in the central absorption component in He\textsc{i} D3, in the red wing of Na\textsc{i} D and the redshifted component of He\textsc{i} D3, the red wing of H\textbeta and finally the red wing of H\alpha. We should emphasize two things. First, these absorption features do not appear at the high velocities characteristic of free-fall. This is consistent with viewing SU Aur close to edge-on, i.e. under a small angle with the plane of the disk; hence the line-of-sight always makes a considerable angle with the base of the accretion flow probably at high latitudes on the star. Second, the time-lagged behaviour that we observe cannot be due to time-variable (non-steady) accretion, because in that case the lines that form closer to the disk would be affected first and that is the reverse of what we observe. In the oblique magneto-spheric model, the column density of the accreting matter seen in absorption against the star varies with the viewing phase of the system: at a certain phase we look through the densest parts of the accretion flow, whilst half a rotation later the densest parts are no longer seen in front of the star (see Johns & Basri 1995). In this scenario no time-lagged behaviour will be observed if the magnetosphere co-rotates with the star as a solid axi-symmetric body, due to the radial alignment of the regions of formation of the different spectral lines.

Smith et al. (1999) found a similar sequence of increasing time lags for decreasing Balmer series, on one night of observations, that they attribute to an accretion stream and shock seen as they moved over the limb of the star. However, any such occultation effects will be time-symmetric: if the ingress of a region of enhanced column density is seen subsequentially in spectral lines of different excitation conditions, then the reverse sequence is seen for the egress of that region. As a result, although the duration of eclipse may differ from line to line, the time of mid-eclipse will be equal for all spectral lines. Similarly, the inner regions of the densest part of the accretion flow appear longer in front of the star than the outer regions, but the times of mid-transit are the same.

We propose that the time-lagged behaviour that we observe may occur if the anchors of the magnetic field lines in the star have a higher rotation rate than those in the inner disk. Then the field lines and hence the accretion flow are no longer radial and the time symmetry for ingress/egress of transit (or occultation) events is broken: mid-transit (or mid-eclipse) will occur at different times for spectral lines formed at different distances to the star, causing the observed time lags. This seems also to be supported by a possible increase of modulation period with distance from the star (see Sect. 2.2), suggesting that the inner parts of the accretion disk are rotating slower than the stellar surface. Thus there is an external torque working on the magnetosphere that would wind up the magnetic field lines. Apparently an equilibrium is established between the external torque and the magnetic pressure contained in the azimuthally distorted magnetic field (see below). It would also hint at a somewhat smaller stellar rotation period of P \sim 2.63 days, more easily reconciled with a smaller stellar radius than the usually adopted R_\star \sim 3.6 R_\odot, which is also suggested by recent modelling of the spectral energy distribution (Oliveira et al. 2000).

A time lag \tau \sim 1.67 day separates the variations in the absorption features in the red and blue wing of H\beta. A slightly bigger time lag (1.77 days) is observed between the blue absorption feature in H\beta and the He\textsc{i} D3 line. Both the blueshifted absorption features in H\alpha and Na\textsc{i} D show similar lagged behaviour (time lags of respectively 1.90 and 1.88 day) with respect to He\textsc{i} D3. In the scenario of
the magnetospheric models, these blueshifted absorption features are wind indicators. Thus, the signatures of accretion and disk winds are out of phase. Our CCF calculations indicate a phase shift of about 240°, but, as it can see from Table [1] the peaks are broad and their amplitude relatively small, so this value is very uncertain.

4.2. Comparison with Predictions from Magnetospheric Models

We have investigated several magnetospheric models that appear in the literature and address the issue of differential rotation in magnetosphere and disk. Some models that approach the problem of magnetospheric accretion from the point of view of spin-up/spin-down of the young stars and jet formation are reviewed in Goodson & Winglee (1999 and references therein). They all consider the case of strong magnetic fields (i.e. there is disk truncation) and the physical distinction between them comes from the effective value of magnetic diffusion in the disk. In these models, the different rotation rates of the star and the disk cause the field lines that permeate the disk to become azimuthally twisted and a toroidal component of the magnetic field is created. The ability of the disk to counteract this toroidal component is described by the effective magnetic diffusivity.

For the most diffusive flows, no wrapping up of the magnetic field lines occurs because the field lines can continuously slip through the disk. This is the case for the Ghosh & Lamb (1973) and the Shu et al. (1994) models. According to Ghosh & Lamb all the field lines are closed and they thread the disk up to distant radii. In the Shu et al. model the closed field lines thread only a small, nearly uniformly rotating, region of the disk and outside this region there are open magnetic field lines.

For low magnetic diffusivity, differential rotation between the disk and the star makes the magnetic field lines wrap up and open via a mechanism known as inflation (Lovelace et al. 1993). The inner edge of the disk undergoes oscillations and magnetic reconnection occurs causing accretion episodes; no steady configuration is possible (Goodson & Winglee 1999).

For intermediate diffusivity, once inflation opens the outer magnetic field lines, a steady state can be attained. The inner magnetic field lines remain closed and approximately in co-rotation with the star. The plasma in the disk can move radially inwards until it reaches the point where steady accretion occurs (Lovelace et al. 1993). In this last scenario, it is plausible that the closed magnetic field lines are azimuthally deformed.

The time-lagged behaviour that we observe in SU Aur suggests a quasi-steady configuration, in which the magnetic field lines are azimuthally curved as a result of the magnetic field line anchors being dragged by, but slipping through the inner disk that is rotating somewhat slower than the magnetic field line anchors on the stellar surface. The misalignment of rotation and magnetic axes introduces, at certain phases, an extra magnetic pressure component in the plane of the disk, that eases the loading of the closed magnetic field lines with matter from outside the co-rotation radius.

But how do the outflows relate with this proposed scenario? Our proposed scenario includes open field lines that can drive wind flows (as suggested by Shu et al. 1994). We have found that the signatures of accretion and disk winds are about 240° out of phase. This agrees with the suggestion of Johns & Basri (1995) (confirmed by Petrov et al. 1996) if their picture of the oblique rotator is refined to include azimuthally curved magnetic field lines.

5. Transient Blueshifted Absorption Features

5.1. Velocity Variations

Two transient absorption features were detected in the blue wings of the profiles of Hα, Hβ and Na i D (Unruh et al. 1993). We did not pursue a multi-component analysis of these lines (as done in Giampapa et al. 1993, Johns & Basri 1995, or Oliveira & Foing 1999) due to the optical thickness of the emission and the complexity and dynamics of the profiles. We could however isolate the transient features in the spectra by applying an adequate filtering procedure. The velocity position of the features is determined by detecting the minimum (in a chosen velocity interval) in the difference spectra with respect to the median-filtered spectra. In Fig. 3, the velocity evolution of these features is plotted (features A and B). There is no considerable change in the width/depth of the features, but these measurements are very difficult to carry out due to the intrinsic variability of the underlying profile.

Feature A persisted for about 1.6 days. It drifted from approximately −140 to −90 km s$^{-1}$ in Hα and from −110 to −70 km s$^{-1}$ in Na i D1. In Hβ we cannot identify the velocity position of the feature unambiguously and so the minimum detection was more uncertain. However, there are indications that $|v(Hα)| > |v(Hβ)| > |v(Na i)|$. The velocity evolution in the three lines follows parallel tracks in time. The onset of the feature A is simultaneous with the flux enhancement observed in Hα and Hβ (Sect. 3.2).

Feature A may therefore originate in regions higher in the magnetosphere that contribute little to the Na i D line formation. In Hα this feature drifted from −140 to −80 km s$^{-1}$ and seems to be decaying after 3 days when our time series ends. In contrast to what we observe for feature A, the velocity position of feature B in Hβ is practically the same as in Hα. We stress that feature B is more conspicuous in Hβ. In the case of feature B it is rather difficult to be certain if it is an absorption or emission transient, or a combination of both.
Fig. 6. Velocity evolution of two drifting absorption features in the line profiles of \( \bullet \) H\( \alpha \), \( \odot \) H\( \beta \) and \( \times \) Na\( i \) D1. For Na\( i \) D2 the velocity position of the feature is similar to Na\( i \) D1. Feature B was not detected in Na\( i \) D. Feature A lasts for at least 1.6 days and feature B for 3 days. The velocity position of the features is determined by detecting the local minimum in the line profiles. Simultaneously with feature A, an intensity enhancement was observed in H\( \alpha \) and H\( \beta \), affecting the whole profiles.

5.2. Interpretation: Sporadic Mass Ejections

We propose that the first transient absorption feature might be plasma ejected upward, that condenses and afterwards decelerates under the influence of gravity, causing the observed velocity evolution. We have investigated several scenarios that could cause such velocity evolution. A blob of matter moving at constant velocity, in which case the velocity variation would be just the result of angular projection, is ruled out because it could not cause the velocity difference between the lines. The same problem is faced when postulating a blob that departs from the stellar surface with the escape velocity and then decelerates. The observed offset between the initial velocities of the lines indicates radially elongated material that underwent an acceleration outwards by an as yet unidentified mechanism, before it started to decelerate. For the second transient feature the velocity evolution shows no evidence of any initial acceleration. Still, as for the first feature, the velocity evolution strongly suggests deceleration even though the dispersion is very large.

We investigated several types of solar-like phenomena that could have similar characteristics. Post-flare loops or surges are out of consideration because, although the matter is initially accelerated and condenses, it then falls back to the solar surface and would thus appear as redshifted absorption features, not blueshifted as we observe. Such redshifted absorption components have been detected on other stars though, e.g. HR 1099 (Foing et al. 1994) and AD Leo (Houdebine et al. 1993) and were proposed to be the analogue of post-flare loops.

If the deceleration measured for feature A is interpreted as gravitational deceleration of material, then a fit to that deceleration rate indicates a location of the decelerating matter at approximately 7 to 8 R\( \ast \). It is difficult to explain a column of material progressing at such distances from the star, specially without knowledge of its previous evolution.

Feature A might be the line-of-sight absorption of material of a large scale coronal mass ejection, in a configuration sometimes called a halo mass ejection. Similar to what is believed to happen in the Sun and flare stars (Foing 1989; Houdebine et al. 1993), a disruption of the magnetic field lines, perhaps near the truncation radius, might cause a “forward” mass ejection, away from the star, that cools and condenses and is observed as transient absorption features, and a “backwards” release of matter/energy, that can hit the star and cause the Balmer brightening we observe. In the case of SU Aur, these ejections clearly point at a magnetospheric connection between the star and the disk where magnetic stresses and energy build up and are released sporadically. To reproduce the time evolution of the flare, as seen in the Balmer brightening, (peak at day 9.1, Fig. 3) and of the decelerated absorption component (start at day 8, Fig. 6), we suggest that the primary instability and energy release did not occur at the stellar surface or in the lower atmosphere, but rather at high altitude in the interacting magnetosphere between the star and the disk. For the second absorption feature, a similar scenario would apply, but without a visible detection of a flare.

The events that we observed are very likely triggered by magnetic field disruption, perhaps in the context of sheared magnetic field lines as described in the previous section. The energy released during these events, in combination with more continuous energy release from magnetic field reconfiguration, might explain the especially high X-ray luminosity of SU Aur (Skinner & Walter 1998).
6. Summary

The circumstellar environments of CTTS are extremely interesting for studying the interaction between the star and the disk. The CTTS line profiles are very complex and diverse, as both accretion and outflows play a role in their formation. In this paper we try to disentangle to some extent these effects, by analysing Hα, Hβ, Na i D and He i D3, in an attempt to constrain the geometry and dynamics of the magnetosphere.

The He i D3 line in SU Aur has two components. Their variability is slightly time-lagged, indicating spatially displaced regions of formation. The component at rest velocity can be formed close to or at the stellar surface, for instance in the post-shock region, and the redshifted component in the accretion column. We propose that the redshifted component of He i D3, the red wings of Na i D and the redshifted absorption features in Hβ and Hα are all formed in the accretion funnel, at different distances from the star according to their opacities and excitation conditions. We find different time lags between these lines, with the variability of the lines closer to the star preceding the variability in the outer spectral lines. We argue that such behaviour cannot be caused by non-steady accretion, nor by simple occultation effects in an oblique magnetospheric model. We propose that such time-lagged behaviour can only occur if the magnetic field lines in the oblique magnetosphere have an azimuthal component.

We find that the near blue wings of Hα, Hβ and Na i D (wind indicators) are out of phase with the accretion indicators, though not exactly in anti-phase.

We observe two transient absorption features in the blue wings of Hα, Hβ and Na i D. The velocity evolution of the first feature indicates matter to be initially accelerated (different velocities for the different lines). Subsequent evolution suggests a deceleration or a projection effect. We propose that these features are the signature of plasma outflow events, powered by the disruption of the distorted magnetic field lines.

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Appendix A: Cross-Correlation Function Analysis

A.1. Definition and Computational Method

Let us assume two stationary time series L1(t) and L2(t) discretely sampled N times at times t_i, with Δt = t_{i+1} − t_i for all values 1 ≤ i ≤ N − 1. The cross-correlation function (CCF), computed at intervals τ (or time lags) which are integer multiples of the sampling interval Δt, is defined as follows:

\[ CCF(\tau) = \frac{1}{N} \sum_{i=1}^{N-1} \frac{[L_1(t_i) - \bar{L}_1][L_2(t_i + \tau) - \bar{L}_2]}{\sigma_1 \sigma_2} \]  

(A.1)

where \( \bar{L}_k \) and \( \sigma_k \) are respectively the mean and standard deviation of each time series L_k(t_i). The obvious problem is that our time series is unevenly spaced, so this definition has to be adapted.

There are two methods to circumvent this difficulty: the interpolation method and the discrete correlation function. In the first method (Gaskell & Peterson 1987), the CCF is calculated twice for each time lag τ: the observed points L_1(t_i) are correlated with the interpolated values of L_2(t_i − τ) and the observed points L_2(t_i) are correlated with the interpolated values L_1(t_i + τ). The two results are then averaged, assuming there is no reason to prefer one interpolation over the other. The second method, the discrete correlation function (DCF) was introduced by Edelson & Krolik (1983). In this method the cross-correlation function is computed at each time lag using only real data points separated by τ. The resulting correlation function is then binned on intervals δτ so that the calculated value at time lag τ is an average over the interval τ ± δτ/2.

These methods were found to be in good agreement for well sampled data sets with a large number of data points (White & Peterson 1994, henceforth WP, and references therein). The DCF method is more general in the sense that it makes no assumptions on the nature of the time series that we are sampling. When using the interpolation method, it is assumed implicitly that the sampled time series vary smoothly on the time scales that correspond to the intervals between observations. Still, the DCF will require more points than the interpolation method to give a meaningful result and, in the limit of poor sampling, will more easily fail to give a significant lag. Therefore, for our data set we decided that the interpolation method is more adequate and hence used this in the calculations presented in this paper.

A.2. Optimization Techniques

When calculating the CCF for several types of test functions with the same time sampling as our data points, we realised that the calculations yielded CCF peak values above unity. There was clearly a normalization problem in the calculation of the CCF. For stationary time series, the mean and variance of the sample are invariant in time; only in this situation it is valid to calculate \( \bar{L}_k \) and \( \sigma_k \) using
the entire time series. We have concluded that this is not always a reasonable assumption: in fact, in our data set there was a strong flux enhancement in the spectral lines (Sect. 3.2), so clearly these statistical quantities change in time. Thus, we concluded that it was more appropriate to compute $T_k$ and $\phi_k$ for each lag $\tau$, with only the data points effectively used for the computation of $CCF(\tau)$. Therefore, the calculation of $CCF(\tau)$ reduces to the calculation of the linear correlation coefficient at each lag $\tau$.

We address now the question of how the interpolation is actually performed. First, following WP, we do not interpolate beyond the limits of the time series: we exclude from the calculation of $CCF(\tau)$ points where $t_i - \tau < t_1$ or $t_1 - \tau > t_N$. We also use linear interpolation of the data points (WP). As it is mentioned above, the interpolation assumes that the times series vary smoothly between the sampled data points. In our time series the extreme data points are separated from the rest of the observations by more that 1.5 days. We have computed the $CCF$ both including and excluding these points and we concluded that the $CCF$ peaks are much sharper in the last case. So we have excluded those data points from $CCF$ calculation, even though we still use them for the calculation of the interpolated series. We should point out that the number of points used is only decreased to $N - 4$.

As we have mentioned the sampling of $H\beta$ is worse: we have only 72 $H\beta$ spectra against 126 for the remaining lines. The calculated $CCF(\tau)$ is an average quantity if there is no reason to favour one of the interpolations. But if we are interpolating $H\beta$ and $H\alpha$, for example, it is clear that the interpolation of the $H\alpha$ series is better because it is computed with more data points. Thus, when a $CCF$ that involves $H\beta$ is computed we will consider only one term, the one where the other time series is interpolated. In the example above we consider only the terms where the interpolated $H\alpha$ series is cross-correlated with the observed $H\beta$ series.

A.3. Error Analysis

Gaskell & Peterson [1987] propose an analytical formula to compute the uncertainty of the time lag $\tau$. WP and Maoz & Netzer [1989] found that this formula can severely underestimate the uncertainties. Accordingly, we have decided to use Monte Carlo simulations to estimate these errors. We assume that the noise in our time series has a gaussian distribution. We use the standard deviation of the continuum as a conservative estimate of the noise in the spectral lines. We computed the $CCF$ with a sampling step of $\Delta \tau = 0.025$ day (approximately half of the maximum exposure time in the time series). We used 1000 trials for the simulations. We then computed the empirical cross-correlation peak distribution ($CCPD$) (Maoz & Netzer [1989]), by simply counting how many times the peak occurred at each time lag. The peak of the $CCPD$ is the most likely time lag and its width is the uncertainty of this estimate. Given the asymmetry of the $CCPD$, we follow WP and define the quantity $\pm \Delta \tau_{67}$, for which 2/3 of the trials give a lag in the interval $\tau \pm \Delta \tau_{67}$ with relation to the median of the distribution. When the $CCPD$ is a gaussian $\Delta \tau_{67}$ corresponds to the standard deviation. The quantity $\Delta \tau_{67}$ is derived directly from the cumulative $CCPD$.

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