Weight Divergence Driven Divide-and-Conquer Approach for Optimal Federated Learning from non-IID Data

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Abstract
Federated Learning allows training of data stored in distributed devices without the need for centralizing training data, thereby maintaining data privacy. Addressing the ability to handle data heterogeneity (non-identical and independent distribution or non-IID) is a key enabler for the wider deployment of Federated Learning. In this paper, we propose a novel Divide-and-Conquer training methodology that enables the use of the popular FedAvg aggregation algorithm by overcoming the acknowledged FedAvg limitations in non-IID environments. We propose a novel use of Cosine-distance based Weight Divergence metric to determine the exact point where a Deep Learning network can be divided into class agnostic initial layers and class-specific deep layers for performing a Divide and Conquer training. We show that the methodology achieves trained model accuracy at par (and in certain cases exceeding) with numbers achieved by state-of-the-art Aggregation algorithms like FedProx, FedMA, etc. Also, we show that this methodology leads to compute and bandwidth optimizations under certain documented conditions.

1. Introduction
Federated Learning has been proposed as a new learning paradigm to overcome the privacy regulations and communication overheads associated with central training (McMahan et al., 2017)(Li et al., 2020). In Federated Learning, a central server shares a global model with participating client devices and the model is trained on the local datasets available at the client device. The local dataset is never shared with the server, instead, local updates to the global model are shared with the server. The server combines the local updates from the participating clients using an Optimization (or Aggregation) Algorithm and creates a new version of the global model. This process is repeated for the required number of communication rounds until the desired convergence criteria are achieved.

Federated Learning differs significantly from traditional learning approaches in terms of optimization in a distributed setting, privacy preserving learning, and communication latency during the learning process (Bonawitz et al., 2019). Optimization in Distributed setting differs from the traditional learning approach due to statistical and systems heterogeneity (McMahan et al., 2017). The statistical heterogeneity manifests itself in the form of non-independent and identical distribution (non-IID) of training data across participating clients. The non-IID condition arises due to a host of reasons that is specific to the local environment and usage patterns at the client. Causes for the skewed data distribution have been surveyed extensively and it has been proven that any real-world scale deployment of Federated Learning should address the challenges around non-IID data. A good example specific to the medical domain can be found in (Xu & Wang, 2020). Several approaches have been studied to address the non-IID heterogeneity. Data Distillation which involves sharing of client data with central server (Zhao et al., 2018) (Lin et al., 2020), Client specific local models or Personalization layers to customize the last few layers of the global model specific to the client data (Fallah et al., 2020) (Ghosh et al., 2020) (Hanzely et al., 2020) (Dinh et al., 2020) (Hanzely & Richtárik, 2020), Novel optimization algorithms (McMahan et al., 2017) (Sahu et al., 2020) (Wang et al., 2020) (Chen et al., 2020) etc. are some of these most researched approaches.

Data Distillation techniques violate the strict privacy requirements. Client specific model approach results in multiple models, which does not cater to any specific requirement for a single model for deployment. In this paper, we focus on the Optimization Algorithm approach to address the non-IID challenge. While there are numerous state-of-the-art algorithms like FedProx (Sahu et al., 2020), FedMA (Wang et al., 2020), FedMAX (Chen et al., 2020) etc., these approaches are not productized in a large scale to the best of knowledge of the authors. Hence, we focus on the most widely deployed FedAvg algorithm (McMahan et al., 2017)
and investigate improving its ability to handle non-IID data to the same level as state-of-the-art algorithms like FedMA, FedProx, FedMAX, etc.

The primary contribution of this paper is proposing a novel Divide-and-Conquer training methodology which in combination with FedAvg is able to meet state-of-the-art performance in simulated environment. Another contribution of this paper is the novel use of the Cosine Distance based Weight Divergence metric to partition the global model into class agnostic initial layers and class-specific deep layers. The two parts of the global model are trained in a mutually exclusive manner while freezing the other part. Under certain documented conditions, this approach also leads to better compute and bandwidth optimization.

The rest of the paper is organized as follows. Section II discusses the limitation with vanilla FedAvg algorithm while section III explains the Divide-and-Conquer methodology. We document the simulation environment, experiments, and results in the simulated environment in section IV establishing the state-of-the-art credentials of the approach. Finally, we conclude the paper and discuss possible future work in section V.

2. FedAvg and its Challenges

Federated Learning (FL) methods are designed to train over multiple devices, each holding their own data, with a central server driving the global learning objective across the entire network. The standard formulation of FL aims to find the minimizer of the overall population loss (Sahu et al., 2020) shown below.

\[
\min_w f(w) = \sum_{k=1}^{N} p_k F_k(w) = \mathbb{E}_k[F_k(w)],
\]

where \( N \) is the number of devices, \( p_k \geq 0 \), and \( \sum_k p_k = 1 \).

In general, the local objectives measure the local empirical risk over possibly differing data distributions with samples available at each device. In a non-IID environment, the assumption of a global minimizer being representative of the overall population is not valid as every client has its own data distribution which differs from other clients and the overall population. Hence, on each client, a local objective function based on the client’s data is used as a surrogate for the global objective function. At each outer iteration, a subset of devices are selected and local solvers are used to optimize the local objective functions of the selected client. Each client then communicates its local model updates to the central server, which aggregates them and updates the global model accordingly. In addition to the usual hyper-parameters of traditional learning like batch size, optimizer, etc., Federated Learning has additional hyper-parameters like epochs per round \( (E_p) \), number of communication rounds, number of participants in each round, and optimization algorithm which can be tweaked for optimal performance.

In FedAvg, the local objective function at client \( k \) is \( F_k(\cdot) \), and the local solver is the stochastic gradient descent (SGD), with the same learning rate \( (\eta) \) and number of local epochs used on each client. At each round, a subset \( K < N \) of the total clients are selected and run SGD locally for \( E_p \) number of epochs, and then the resulting model updates are averaged. The details are summarized below.

Tuning of the hyper-parameters is a critical requirement for optimal performance of FedAvg. The number of epochs plays a critical role in convergence as more number of epochs leads to faster convergence. This comes at the cost of higher compute on client devices but with the benefit of lower communication. However, the high number of epochs has diminishing returns on the speed of convergence in non-IID conditions. For FedAvg, there is a significant drop in reduction of accuracy due to weight divergence (Zhao et al., 2018). The trade-off between high number of epochs and convergence speed for FedAvg has been addressed in other optimization algorithms like FedProx, FedMA, FedMAX etc. FedProx is very similar to FedAvg but addresses the limitations of the latter by adding a proximal term to client cost functions to limit the impact of local updates within a particular range of global model. This approach allows the number of epochs to be tuned based on the non-IIDness of the client data. While it address the weight divergence issue with FedAvg, the convergence speed is slower at higher number of epochs when compared to other state-of-the-art algorithms (Lin et al., 2020), (Wang et al., 2020) (Chen et al., 2020) (Shoham et al., 2019). FedMA offers the best accuracy and convergence speed in comparison to others but comes with significant compute cost on the client devices. The complexity of this algorithm is also high in comparison with FedAvg or FedProx leading to restrictions on its applicability on certain NN models.

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An ideal optimization algorithm should come with the simplicity and elegance of FedAvg, allow for state-of-the-art accuracy in non-IID environments with comparable or better convergence speed. In this work, we present a novel Federated Training methodology that is well suited to handle non-IID challenges using the simple FedAvg algorithm. Our methodology eliminates performance overheads associated with methods like FedMA while achieving comparable accuracy. Since FedAvg is the de-facto standard in majority production deployments, the proposed method can be easily integrated to offer significant accuracy and convergence benefits with little performance overhead.

Note on the terminology: In the rest of the document, clients will be referred to as collaborators and the server will be referred to as aggregator reflecting the role they play in the overall federation.

3. Divide-and-Conquer Training Methodology

The impact of non-IIDness of data in Federated Learning is well researched in literature. A non-IID data environment leads to over-fitting of local models to the skewed training data at individual collaborators resulting in distortion of previously aggregated feature detectors and descent of SGD optimizer to different local minima at different collaborators.

Typically, the initial layers of a Deep Neural Network (DNN) learn low level or class agnostic features and deeper layers are responsible for learning high level or class-specific features (Zeiler & Fergus, 2014), as illustrated for a vision architecture, VGG9 (Simonyan & Zisserman, 2015), in Figure 1. For training paradigms like Transfer Learning (Reyes et al., 2015), data scarcity mandates the use of special training methods that learn class agnostic features from generic datasets and learn class specific features for any new tasks by freezing the initial layers. This process of decoupling feature-learning and task-learning has been successfully applied to multiple training tasks including recent advances like Few Shot Learning (Yan et al., 2020).

This work extends the idea to Federated Learning to address the challenges with non-IID. Our methodology involves splitting the given DNN into two parts, namely

- Class Agnostic Layers
- Class Specific Layers

The two parts are trained separately. Federated Learning is typically performed using several Communication Rounds (CR), where trained weights from individual collaborators are aggregated together in a central Aggregator. Our proposed method configures collaborators to perform feature-learning and task-learning or fine-tuning in alternate rounds as shown in Figure 2. Weights corresponding to relevant trained layers alone are transferred over to the Aggregator, which results in communication bandwidth reduction. Communication saving is realized during model transfers in both directions (i) Transfer of global models to Collaborators and (ii) Transfer of local trained models from Collaborator to the Aggregator.

Class Agnostic layers, comprised of initial layers of the DNN architecture, are trained more aggressively as com-
Figure 2. Divide and Conquer Training Methodology using alternate Feature-Learning and Fine-Tuning rounds. CR1, C2, represent the communication rounds.

pared to Class-Specific layers. Class Agnostic layer training is treated similar to *feature-learning*. Class Specific layers, consisting of deep layers are trained similar to *fine-tuning*. This ensures that weight divergence across different collaborators, due to non-IIDness of constituent data is minimal and features are insulated from distortion that would otherwise occur due to combined learning of all layers.

While methods like FedProx limit weight divergence, they penalize all layers of the network and hinder learning in Class Agnostic layers. Our approach addresses this by allowing different layers of a network to train differently after grouping initial layers separately from deep layers. Training rounds are configured to alternate between *feature-learning* and *fine-tuning* to facilitate learning under non-IID conditions by freezing relevant layers of DNN architecture. At the beginning of a communication round, the aggregator broadcasts the desired hyper-parameter configurations to collaborators, together with specifications for layers to be frozen. The exact point at which a DNN architecture has to be broken into two parts is decided based on *weight divergence* observed from the pre-pass round of training. The key contributions of our paper can be summarized to the following two key points:

- Novel methodology, called *Divide-and-Conquer*, to train topology in pairs of *feature-learning* and *fine-tuning* steps to handle non-IID conditions.
- Novel use of *weight-divergence* metric, observed from the pre-pass round of training, to split the given DNN topology into Class Agnostic and Class Specific layers. This metric provides a measure of non-IIDness across participating collaborators as a mapping of the layers of DNN architecture they impact the most.

Choice of layers that are chosen for base class *feature-learning* as against novel class *fine-tuning* is a hyper-parameter in *Divide-and-Conquer* training methodology. Few options for splitting the VGG9 topology is shown in Figure 3. For instance, Divide at layer3 assigns layers 1 to 3 for learning class agnostic features and remaining layers for learning class or task specific features. This hyper-parameter is dependent on the *weight-divergence* metric which in turn reflects the non-IIDness of data.

Figure 3. VGG9 : Topology Division and assignment of layers to Feature-Learning and Fine-Tuning Groups

After determining an optimal split, *feature-learning* and *fine-tuning* is achieved by control of other hyper-parameters like number of Epochs ($E_p$) and Learning rate ($\eta$). Fine-Tuning round of learning is scheduled using lower $E_p$ and $\eta$, which is aligned with the conditions under which FedAvg performs the best in non-IID conditions. Federated Learning at a faster pace is achieved by alternating low-level *feature-learning* and high-level *fine-tuning* along with appropriate hyper-parameters as described in the next section.

4. Divide-and-Conquer: Experiments, Results, and Discussion

This section describes the simulation environment, experiments done, and results. The comparison with other state-of-the-art approaches is also captured in the results section to establish the state-of-the-art credentials of our proposed approach.

4.1. Experimental Setup

We present observations from *Divide-and-Conquer* on VGG9 topology using 3 different non-IID conditions as in (Wang et al., 2020), which includes coverage for convolutional layers and LSTMs. Classification and NLP models used were also same as (Wang et al., 2020).

- Classification using Color Skewed CIFAR10 Dataset
FedDnC

(Krizhevsky, 2009): CIFAR10 dataset is split into two groups of 5 classes each, with each class assigned uniquely to the two collaborators. To skew the data further using a 95-5% skew pattern, 95% of images in the first group are converted to gray-scale and 5% of images in the second group are converted to gray-scale. This results in the first collaborator holding gray-scale dominant data and the second collaborator holding color dominant data.

- Classification using Class Imbalanced CIFAR10 Data: Data is distributed non-uniformly across different collaborators to create non-IID conditions from the perspective of total training data per collaborator as well as the number of records per class.

- Next Character prediction model on Shakespeare dataset (Caldas et al., 2018) leveraging non-IIDness in speaking-roles: Data corresponding to each speaking-role in the play is grouped to create unique collaborators, to simulate natural non-IID condition. For the trial, we selected only clients with a minimum of 10k data points and sampled a random subset of 66 clients.

4.2. Hyper-Parameter Selection

4.2.1. Fine Tuning Epoch and Learning Rate

Divide-and-Conquer allows the use of variable hyperparameters for different parts of the network. As discussed earlier, we train feature-learning group more aggressively than fine-tuning group by control of parameters like $E_p$ and $\eta$. Use of lower $E_p$ for fine-tuning rounds results in slightly better accuracy compared to higher epochs. This is because the local models are skewed by over-fitting to non-IID data at the individual collaborators. By using lower values for epoch and learning rate for fine-tuning rounds, we achieve better accuracy while simultaneously reducing compute requirements needed for fine-tuning rounds. Data from Color Skewed distribution is presented in Figure 4. This observation is in alignment with the behavior of FedAvg where a high number of $E_p$ leads to lower training accuracy due to weight divergence.

4.2.2. Topology Division

Depending on the nature and magnitude of non-IIDness, the Class Agnostic and Class Specific layers in a given model will diverge across different collaborators. We explored, weight divergence in the learned model, to guide Divide-and-Conquer (Divide-and-Conquer) methodology. The metric given below was explored in (Zhao et al., 2018).

$$W_d = \frac{||W_1 - W_2||}{||W_1||}$$

Weight divergence from VGG9 model for Color Skewed non-IID simulation described in Section 4.1 is shown in Figure 5. A pre-pass training is initially performed for 5 rounds and layer-wise divergence is computed for future rounds using the pre-pass model as a reference. Model at end of pre-pass comprising 5 rounds is M4. L1, L2 represents different layers of VGG9 while M5, M6, etc., corresponding to models from future communication rounds. Compared to prepass model M4, the divergence is low for the initial set of layers and starts to increase around Layer5. Divide-and-Conquer can be applied around this layer to split the topology for creating feature-training and fine-tuning groups.

To validate the efficacy of $W_d$, Accuracy and convergence behavior for VGG9 under different layer division schemes were checked using a brute force sweep across different splits. Accuracy for different division schemes is presented in Figure 6. As discussed in Section 2, Divide5 corresponds to division after layer5. From the figure, Divide5 offers the best accuracy and convergence speed under the given non-IID condition. All runs used 20 epochs for feature-learning and 4 epochs for fine-tuning. Likewise, learning rate for fine-tuning round was half that of feature-learning. Learning Rate Decay was also applied across the communication rounds starting from 0.001 and reducing by 10% for every round.

For certain division schemes (ex: Divide7), large spread is seen in accuracy between feature-learning and fine-tuning rounds suggesting that the layer assignment strategy for the two groups is sub-optimal. For Divide7, Divide6,
Figure 5. LayerWise Weight Divergence for Color Skewed distribution at different communication rounds. L1,L2 corresponds to layers and M5,M6 corresponds to model at end of successive communication rounds. Divergence is low for initial layers suggesting opportunities for Divide-and-Conquer etc., we find that accuracy is higher for fine-tuning rounds (CR=2,4,6,etc.) and drops for feature-learning rounds (CR=1,3,5,etc.). The trend however reverses for Divide5 where the accuracy is higher for feature-learning rounds and marginally drops for fine-tuning group. The divergence between feature-learning and fine-tuning is also minimal in this split.

When fewer layers are present in feature-learning group as in Divide4, we find that the rate of learning starts to fall and accuracy spread between the two learning groups increases again. This suggests that Divide5 is an optimal split for this topology for this non-IID dataset thereby validating the usage of weight divergence metric to determine the point in a model where the layer split can be performed.

For the Class Imbalanced non-IID condition, the weight-divergence is high across all the layers of the topology [Figure 7], suggesting that Divide-and-Conquer might not offer significant benefits. Accuracy improvements was not seen in brute force sweep across different layer splits as well. For experiment sake, we chose to divide after layer 8 inline with traditional fine-tuning strategies where the last layer is used for fine-tuning. The Next Character prediction model has 3 layers and we again use the last layer for fine-tuning.

In the current work, layer division is determined using a pre-pass run and the scheme is fixed for the entire duration of training. Future work will extend this to explore a dynamic scheme assignment where layers from a group can be reassigned to other group based on observed trend in feature-learning accuracy vs fine-tuning accuracy over few communication rounds.

4.3. Results

Results from the Divide-and-Conquer methodology under different non-IID scenario is presented in this section. For training we use 20 epochs for feature-learning and 4 epochs for fine-tuning. Learning rate was initialized to 0.001 and allowed to decay by 10% for every communication round. Learning rate for fine-tuning was 50% of learning-rate for feature-learning.

Divide-and-Conquer uses half the network bandwidth for data transfers compared to FedAvg, as the full model is transferred for every two communication rounds. For FedMA, results from equivalent matched averaged round is presented based on equivalency established in (Wang et al.,
2020). Though FedMA uses much lower communication bandwidth, compute overhead for layer matching increases with model depth as well as width, making it less desirable for practical deployments. We show that our methodology yields similar accuracy levels as more complex algorithms like FedMA in acceptable rounds of communication. Note: In the tables providing the comparison across different approaches, *Divide-and-Conquer* is captured under *D&C*.

### 4.3.1. Image Classification: Color Skewed Distribution

Training accuracy and convergence profile for different aggregation algorithms using Color Skewed 95-5% CIFAR10 data are shown in Figure 8. It can be seen that for this category of non-IIDness, the model reaches high accuracy with much smaller communication rounds compared to FedAvg. Divide5 was used for this analysis as described in the earlier section along with the same values for $E_p$ and $\eta$. Results for additional levels of Color Skew is presented in Table 1. We chose 18 rounds of communication for the comparison to align with FedMA.

![Figure 8. Accuracy Comparison for Color Skewed Distribution with 95-5% skew.](image)

| #COL | SKEW   | FEDAVG | FEDPROX | FEDMA | D&C  |
|------|--------|--------|---------|-------|------|
| 2    | 95-5%  | 53.1%  | 56.2%   | 81.0% | 80.1%|
| 2    | 75-25% | 52.8%  | 74.6%   | 78.8% | 79.2%|
| 2    | 50-50% | 49.1%  | 67.2%   | 79.9% | 81.8%|

### 4.3.2. Image Classification: Class Imbalance Distribution

For Class Imbalanced data, the observed weight divergence from the pre-pass run was high for most layers. This indicates that *Divide-and-Conquer* does not offer any advantages over FedAvg. As an experiment, we divided the topology at layer8 similar to traditional fine-tuning. *Divide-and-Conquer* yields slightly lower accuracy compared to FedAvg and FedMA as documented in table [2]. However, if bandwidth saving is not considered as a requirement and *Divide-and-Conquer* is run for additional rounds to get a similar amount of model transfer as FedAvg, the performance of *Divide-and-Conquer* is marginally better. This is captured in the table under the column *D&C’*. Though FedMA achieves its accuracy levels using much lower communication bandwidth, compute overhead for layer matching increases with model depth as well as width, as discussed earlier, making it less desirable for practical deployments.

Given the results, it is clear that in cases where weight divergence suggests no clear split layer, it is recommended not to adopt *Divide-and-Conquer*. As collaborator count increases, training data per collaborator decreases in the simulation environment, as the data is divided across the collaborators. This could also lead to increased divergence when feature-learning is done aggressively on sparse data. In a truly federated set up with a large training corpus across collaborators, we expect our methodology to offer better accuracy improvements.

![Table 2. Accuracy for Class-Imbalanced Distribution for 18 communication rounds using 5 & 10 collaborators.](image)

| #COL | FEDAVG | FEDPROX | FEDMA | D&C  | D&C’ |
|------|--------|---------|-------|------|------|
| 5    | 88.5%  | 87.5%   | 87.5% | 87.1%| 89.3%|
| 10   | 83.5%  | 80.0%   | 82.5% | 76.8%| 82.2%|

An extreme case of Class Imbalance based heterogeneity is when each collaborator exclusively holds data from one unique class. All the tested algorithms performed poorly (accuracy less than 15%) under this scenario, suggesting a need for more research in this area.

### 4.3.3. Next Character Prediction: Speaker-Role Based Non-IID Distribution

Results from application of *Divide-and-Conquer* to a character prediction model is shown in table 3. At end of 9 communication rounds, the accuracy from *Divide-and-Conquer* is comparable to other algorithms while only requiring half
the amount of data transfer as FedAvg. 9 rounds of communication was chosen to align with FedMA.

Table 3. Accuracy for next-character prediction lstm model for 9 communication rounds using 66 collaborators. Accuracy from D&C (using FedAvg) is inline with other algorithms

| COL  | FedAvg | FedProx | FedMA | D&C |
|------|--------|---------|-------|-----|
| 66   | 50.8%  | 44.6%   | 47.4% | 49.6% |

5. Conclusion

In this work, we presented a weight divergence based Divide and Conquer algorithm which builds on popular FedAvg algorithm to achieve state-of-the-art accuracy under non-IIDness. By training network in parts, our novel methodology is shown to a) Achieve faster convergence when low-level features are well-represented b) Reduce communication by half, as a consequence of training and weight exchange in parts, and c) Require less compute compared to state-of-the-art techniques like FedMA, which has performance overheads from weight matching. Future work can explore a dynamic Divide-and-Conquer strategy where layers are moved between feature-learning and fine-tuning groups based on accuracy observations during training. Future work can also explore the application of Divide-and-Conquer methodology to learning paradigms like Few Shot Learning to identify Class Agnostic layers for the backbone network.

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