COSMOLOGICAL IMPLICATIONS OF GALAXY CLUSTERS:
BEST-FIT MODELS

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The galaxy cluster power spectrum and mass/temperature functions are currently the most precise observational tools for constraining the theory of the formation of large scale structure (LSS) in the Universe. Complementing these tests by the observational data at larger (cosmic microwave background anisotropy (CMB)) and smaller (distribution of Lyα clouds) scales opens the way to a straightforward determination of the cosmological parameters in simplest dark matter (DM) models. We argue that such a 'minimal data set' is free from systematic effects and can indicate quite precisely the parameters of spatially flat mixed DM model with a positive cosmological constant and no cosmic gravitational waves.

1 Introduction

Three lessons from the galaxy cluster physics are often implied in building-up the true cosmology directly from observations:

- the cluster abundance test (the famous $\sigma_8$ argument or cluster mass/temperature function from data at $z \sim 0$),
- the cluster power spectrum (the distribution of clusters in space),
- the cluster evolution test (the cluster abundance vs redshift).

While the latter still requires better statistics and cluster mass determination, the first two are considered today as the most precise cosmological tests related straightforwardly to the linear density perturbation field which gave the birth to LSS in the Universe (see the review papers at this Conference).

A good concordance of the power spectrum of galaxy clusters in the range $k \in (0.03, 0.2)h$/Mpc reconstructed from different optical and X-ray data (e.g. the talk of P.Schuecker at this Conference and refs therein) evidences a low level of possible systematic uncertainties in cluster data and encourages to apply the $\chi^2$ minimization method for the restoration of the cosmological parameters in simplest DM models.

Certainly, few additional tests have to be taken into account to cover a broader range of scales and, thus, to improve the stability of the method and perform a more comprehensive analysis. However, the danger may arise here in possible introduction of the unclear systematics brought by additional tests, that often makes the result of the analysis dependent on a set of the selected data.
2  Minimal Data Set

The determination of cosmological parameters from some geometrical tests and numerous LSS observations has been carried out in many papers. Though the results are always stable for the prediction of a small matter abundance ($\Omega_m < 1$), the concrete values of $\Omega_m$ and other cosmic parameters leave something to be desired depending strongly on both a family of the theoretical models chosen (the number of free parameters) and a set of observations taken for the analysis. Under such a situation it is tempting to form the current ‘minimal data set’ suffering less from the systematic effects, and to see if the selected data are mutually in agreement implying the same cosmological parameters.

The modern status of observational cosmology prompts to clearly indicate at least three scale regions which have to be taken into account for the problem to be solvable:

- very large scales ($\sim 1000h^{-1}\text{Mpc}$),
- LSS scales ($\sim 10 – 100h^{-1}\text{Mpc}$), and
- small (sub-megaparsec) scales.

Fortunately, all these three levels can be suggested today by the ‘most trustable’ available data related to the primordial density perturbation field through simple linear integrals:

- the first group – by COBE 4-year data,
- the second – by a group of LSS data selected below, and
- the third – by data on the power and distribution of $\text{Ly}_\alpha$ clouds.

If the first and third groups are monopolic (few observational points in each group) destined just to stabilize the spectrum amplitudes in the asymptotic scale regions, then the central (second) group is the most important for the analysis allowing for a subtle ‘fine tuning’ of the result. This group contains a bulk of observational points determining both the spectral slopes and amplitudes within the LSS scales. Novosyadlyj et al. suggested the following seven data points (in the second group) which meet common agreements in literature and can be thought of as ‘most trustable’ and accurate:

- the $\sigma_8 – \Omega_m$ relation found by cluster abundance at $z \sim 0$ (one point),
- the mean peculiar velocity of galaxies in a sphere of radius $50h^{-1}\text{Mpc}$ (one point),
- the Abell-ACO cluster power spectrum in scales $k \in (0.03, 0.2)h/\text{Mpc}$ (three effective degrees of freedom),
- the amplitude and position of the first acoustic peak in $\Delta T/T$ spectrum (two points).

These data points have been shown to be self-consistent (excluding some points from the searching procedure results only in a change of the best-fit parameter values within the range of their corresponding standard errors, see Sections 3,4). More of that, some other data (e.g. the evolution of cluster number density, see Section 4) can be added to these seven points with a no change of the result.

Below we present the cosmological models and constrain the parameters using only this ‘minimal data set’. The reported analysis does not include observations of distant supernovae, galaxy power spectra, a bulk of the CMB data (except the two mentioned points for the location and position of the first acoustic peak and the COBE normalization), the local measurements of Hubble constant, the age of globular clusters, the evolution tests and some other data. It is interesting to see if and how our result confronts with these ‘other’ observational tests mentioned.
The usual cosmological paradigm – a scale free power spectrum of scalar primordial perturbations which evolve in a multicomponent medium to form the large scale structure of the Universe – is compatible with the observed LSS and CMB data. Most inflationary scenarios predict a scale free primordial power spectra of scalar density fluctuations \( P(k) \sim k^n \) with arbitrary \( n \) as well as gravity waves which contribute to the power spectrum of CMB temperature fluctuations \( \Delta T^2 \ell \) at low spherical harmonics. But models with a minimal number of free parameters, such as the scale invariant \( (n = 1) \) standard cold DM model or the standard mixed (cold + hot) DM model are excluded by observational data.

Better agreement between theory and observations can be achieved in models with a larger number of parameters: cold dark matter (CDM) or mixed dark matter (MDM) with baryons, a tilted primordial power spectra, spatial curvature, cosmological constant, and a tensor contribution to the CMB anisotropy power spectrum. However, to ensure a better stability and convergence of the minimization method on the basis of the ‘minimal data set’, the total number of free parameters in the model should not be large (currently, not exceeding ten).

One way to improve the standard MDM is an introduction of cosmic gravity waves (CGW). However, the direct approach (just introducing the tensor mode while keeping the \( \Lambda \)-term vanishing) is not effective (see Mikheeva et al.): the best-fit model normalized by \( \sigma_8 \) and COBE data requires too much hot matter (\( \Omega_\nu \geq 0.2 \)) and too low first acoustic peak (inconsistent with \( L_y_\alpha \) and CMB observations). Another way – the introduction of cosmological constant without CGW – appears more powerful.

Novosyadlyj et al have performed such an analysis for \( \Lambda \)MDM spatially flat cosmological model (\( \Omega_\Lambda + \Omega_m = 1 \)) without tensor mode, also neglecting a possible effect of the early reionization which could reduce the amplitude of the first acoustic peak in the CMB anisotropy spectrum. The reason for the restriction of flat models is strongly motivated by the results from the BOOMERANG experiment whereas neglecting the CGW and reionization is mainly technical: the extraction of these parameters in models with non-zero \( \Lambda \)-term would require more accurate experimental data than those available today.

Among the free cosmological parameters one is discrete (the number of species of massive neutrinos) and six are continuous within the following ranges:

- \( N_\nu = 1, 2, 3 \), the number of massive neutrino species,
- \( n \in (0.7, 1.4) \), the tilt of primordial spectrum,
- \( \Omega_m \in (0, 1) \), the abundance of total matter,
- \( \Omega_\nu \in (0, 0.4) \), the abundance of hot matter,
- \( \Omega_b \in (0, 0.2) \), the abundance of baryons,
- \( h \in (0.4, 0.8) \), the Hubble constant in units \( 100 \text{km s}^{-1} \text{Mpc}^{-1} \),
- \( b_{Cl} \in (1, 5) \), the bias of galaxy cluster distribution.

The abundance of cold dark matter and cosmological \( \Lambda \)-term are found from the equations \( \Omega_c = \Omega_m - \Omega_\nu - \Omega_b \) and \( \Omega_\Lambda = 1 - \Omega_m \), respectively; the bias of the cluster power spectrum with respect to the dark matter distribution is supposed to be linear and scale independent in the range of scales considered.

The method for detecting cosmological parameters from the ‘minimal data set’ has been tested for the stability with help of the constructed mock sample of observational data. The only poorly determined parameter (from the LSS data alone) turned out to be the baryonic
abundance. To fix $\Omega_b$ with better accuracy we have added a single geometrical test in our analysis: the Big Bang nucleosynthesis constraint, $\Omega_b h^2 = 0.019 \pm 0.0024$. With such an addition the method reveals as very stable and finds all the parameters of 'true' model whenever possible.

The best-fit model with the minimum of $\chi^2$ (when all parameters are free) is presented in the first line of Table 1. The rest eleven lines display some other best-fit models (with some of the seven parameters fixed) which have got within the 1$\sigma$ contour (from the first-line model). In all the models $\chi^2_{\text{min}}$ is in the range

$$N_F - \sqrt{2N_F} \leq \chi^2_{\text{min}} \leq N_F + \sqrt{2N_F}$$

which is expected for a Gaussian distribution with $N_F$ degrees of freedom (the number of observational points minus the number of free model parameters).

Table 1: Cosmological parameters of $\Lambda$MDM models without cosmic gravity waves (the free/fixed parameters are given with/without standard errors)

| No | $N_\nu$ | $\chi^2_{\text{min}}$ | $n$ | $\Omega_m$ | $\Omega_\nu$ | $\Omega_b$ | $h$ | $b_{cl}$ |
|----|--------|-----------------|----|------------|-------------|------------|----|-------|
| 1  | 1      | 4.63            | 1.12±0.10 | 0.41±0.11 | 0.059±0.028 | 0.039±0.014 | 0.70±0.12 | 2.23±0.33 |
| 2  | 2      | 4.80            | 1.13±0.10 | 0.49±0.13 | 0.103±0.042 | 0.039±0.014 | 0.70±0.13 | 2.33±0.36 |
| 3  | 3      | 5.07            | 1.13±0.10 | 0.56±0.14 | 0.132±0.053 | 0.040±0.015 | 0.69±0.13 | 2.45±0.37 |
| 4  | 1      | 5.27            | 1.12±0.09 | 0.51±0.07 | 0.074±0.041 | 0.053±0.003 | 0.60   | 2.43±0.26 |
| 5  | 1      | 4.65            | 1.12±0.10 | 0.39±0.05 | 0.058±0.026 | 0.037±0.002 | 0.72   | 2.19±0.23 |
| 6  | 1      | 12.23           | 1.07±0.09 | 1.00      | 0.116±0.086 | 0.118±0.027 | 0.40±0.05 | 3.15±0.39 |
| 7  | 2      | 10.17           | 1.10±0.09 | 1.00      | 0.177±0.086 | 0.099±0.022 | 0.44±0.05 | 3.10±0.38 |
| 8  | 3      | 8.80            | 1.12±0.09 | 1.00      | 0.219±0.084 | 0.085±0.019 | 0.47±0.05 | 3.07±0.38 |
| 9  | 1-3    | 6.54            | 1.04±0.10 | 0.30      | 0.000±0.005 | 0.038±0.013 | 0.71±0.12 | 2.25±0.19 |
| 10 | 1      | 6.18            | 1.00      | 0.45±0.12 | 0.042±0.032 | 0.038±0.014 | 0.71±0.13 | 2.44±0.31 |
| 11 | 3      | 10.43           | 1.00      | 1.00      | 0.159±0.069 | 0.075±0.021 | 0.51±0.07 | 3.23±0.35 |
| 12 | 1-3    | 6.92            | 1.00      | 0.30      | 0.000±0.010 | 0.034±0.009 | 0.75±0.10 | 2.25±0.20 |

4 Results and Discussion

As it is seen from Table 1, the considered observational data on LSS of the Universe can be explained by a flat $\Lambda$MDM inflationary model with a tilted spectrum of scalar perturbations and vanishing tensor contribution. The best fit parameters are: $N_\nu = 1$, $n = 1.12 \pm 0.10$, $\Omega_m = 0.41 \pm 0.11$, $\Omega_\nu = 0.059 \pm 0.028$, $\Omega_b = 0.039 \pm 0.014$ and $h = 0.70 \pm 0.12$. The CDM density parameter is $\Omega_c = 0.31 \pm 0.15$ and $\Omega_\Lambda$ is considerable, $\Omega_\Lambda = 0.59 \pm 0.11$.

If all parameters are free (line 1) the model with one sort of massive neutrino provides the best fit to the data. However, there are only marginal differences in $\chi^2_{\text{min}}$ for $N_\nu = 1, 2, 3$ (lines 1,2,3, respectively), therefore, with the given accuracy of the data we cannot currently conclude whether – if massive neutrinos are present at all – their number is one, two, or three.

The spectral index is close the Harrison-Zel’dovich and coincides with the COBE prediction. The neutrino matter density is about the baryon abundance: $\Omega_\nu \sim \Omega_b \sim 10\%$ of $\Omega_m$.

Surprisingly, the prediction of model parameters from the 'minimal data set' is consistent with observations of the nearby and distant SNIa, the age of globular clusters, and the existence
of rich galaxy clusters at $z \geq 0.5$. However, the comparison with galactic power spectra creates a problem since different systematics in galaxy catalogues and a scale-dependent bias because of non-linear clustering of galaxies at small scales.

Notice, that the value of Hubble parameter found from the LSS tests is consistent with local measurements of Hubble constant. It is interesting to see that the value of Hubble constant anticorrelates with the total matter abundance (lines 4,5): roughly, the production of both factors remains constant, $\Gamma \equiv \Omega_m h \simeq 0.3$. Note, that without hot matter ($\Lambda$CDM) $\Gamma \simeq 0.22$ (see lines 9,12) in concordance with other results.

Furthermore, increasing the number of massive neutrino species from 1 to 3 leads to an increase of $\Omega_\nu$ from 0.06 to 0.13 and to a decrease of $\Omega_\Lambda$ from 0.59 to 0.44 (lines 1,2,3). The correlation between $\Omega_\nu$ and $\Omega_m$ can be approximated at the 'maximum likelihood ringe' by the following equation:

$$\Omega_\nu \simeq 1.3\Omega_m^2 - 0.44\Omega_m + 0.023$$

There are some other interesting models staying within the 1$\sigma$ range form the best-fit first line. Among them are the matter dominated models with zero $\Lambda$-term (lines 6,7,8): all these models require rather high abundance of the hot matter (up to 22% for three sorts of massive neutrino) and extremely low value of the Hubble constant ($h < 0.5$) which is in obvious disagreement with the local SNIa measurements.

The models with low $\Omega_m \sim 0.3$ (lines 9,12) fit the observational data somewhat less good than the best model ($\Delta\chi^2_{min} \simeq 2$) but all predictions are still within the 1$\sigma$ contour. Such model prefers a high Hubble parameter ($h \gtrsim 0.7$) and no massive neutrinos. Obviously, it is the standard $\Lambda$CDM.

Concerning the perfectly scale invariant primordial power spectrum (lines 10,11,12), these models prefer $\Lambda$MDM (with a somewhat lower neutrino content than in the best-fit model in line 1) if the remaining parameters are initially free (line 10), and the $\Lambda$CDM if the matter content is initially fixed as low (line 12). As for the matter dominated model with $n = 1$ (line 11), it is just the standard MDM with a low Hubble parameter, $h \simeq 0.5$, practically coinciding with the line 8.

If the hot component is eliminated from the very beginning or $\Omega_\nu$ is fixed at the small value defined by the lower limit of the neutrino mass $\sqrt{\delta m^2_{\nu}} = 0.07$ from the Super-Kamiokande experiment, $\Omega_\nu = 7.4 \times 10^{-4}$, we obtain the best-fit value for the matter density parameter $\Omega_m \simeq 0.39 \pm 0.11$ and the Hubble constant $h = 0.62 \pm 0.12$.

The errors in the best fit parameters presented in Table 1 are the square roots of the diagonal elements of the covariance matrix. More information about the accuracy of the determination of parameters and their sensitivity to the data used can be obtained from the contours of confidence levels presented in Fig. 1. These contours show the confidence regions which contain 68.3% (solid line), 95.4% (dashed line) and 99.73% (dotted line) of the total probability distribution in the two dimensional sections of the six-dimensional parameter space of $\Lambda$MDM models, if the probability distribution is Gaussian.

As one can see in Fig.1a the iso-$\chi^2$ surface is rather prolate from the low-$\Omega_m$ - high-$n$ corner to high-$\Omega_m$ - low-$n$. This indicates some degeneracy in $n - \Omega_m$ parameter plane, which can be expressed by the following equation which roughly describes the ‘maximum likelihood ridge’ in this plane within the 1$\sigma$:

$$n\sqrt{\Omega_m} \simeq 0.73$$

A similar degeneracy in the $\Omega_\nu - \Omega_m$ plane in the range $0 \leq \Omega_\nu \leq 0.17$, $0.25 \leq \Omega_m \leq 0.6$ (Fig.1c) was already discussed above. The both degeneracies have clear physical explanation. The rest contours are quasi-spherical and consistent with the Gaussian character of the errors.

One important question is how each point of the data influences the final result. To estimate this we have excluded some data points from the searching procedure. Excluding any part of
Figure 1: The likelihood contours (solid line - 68.3%, dashed - 95.4%, dotted - 99.73%) of the tilted ΛMDM model with $N_\nu = 1$ and parameters from Table 1 (line 1) in the different planes of $n - \Omega_m - \Omega_\nu - \Omega_b - h$ space. The parameters not shown in a given diagram are set to their best fit values.
Figure 2: The observed Abell-ACO power spectrum (filled circles) and the theoretical spectra predicted by tilted ΛMDM models with parameters taken from Table 1 ($N_\nu = 1$).

Observe results only in a slight change of the best-fit values of $n$, $\Omega_m$, and $h$ within the ranges of their corresponding standard errors. This indicates that the data are mutually in agreement implying the same cosmological parameters (within the error-bars). Concerning the parameter $\Omega_\nu$, a very important is the small scale constraint: the $L_{\gamma\alpha}$ tests reduce the hot dark matter content from $\Omega_\nu \sim 0.22$ to $\sim 0.07$. The rest tests stabilize the value of $\Omega_\nu$ within its still considerable errorbars.

The most crucial test for the baryon content is of course the nucleosynthesis constraint (LSS alone does not determine $\Omega_b$). Its $\sim 6\% - 1\sigma$-accuracy safely keeps $\Omega_b h^2$ near its median value 0.019. The parameter $\Omega_b$ in turn is only known to $\sim 36\%$ accuracy due to the large errors of other experimental data (reduced to the uncertainty in Hubble constant). The obtained accuracy of $h$ ($\sim 17\%$ from the 'minimal data set') is better than the one assumed from direct local measurements ($\sim 23\%$ only).

Thus, all the data points used in the analysis are non-contradictory and mutually self-consistent: all they are important for searching the best-fit cosmological parameters.

Finally, let us emphasize an important spectrum property. The experimental Abell-ACO power spectrum and the theoretical predictions for some best-fit models are shown in Fig. 2. As we see the best-fit spectra do not have any peculiarity at the scale $k \sim 0.05h/\text{Mpc}$. More of that, the theoretical spectra bend evidently at larger scale! This can create a problem for ΛMDM: if better data on the spatial distribution of galaxy clusters will confirm the presence of the bent/feature in the power spectrum the whole ΛMDM paradigm will be in trouble. A way out could be that the real spectrum bent occurs at larger scale, $k_{\text{bent}} \leq 0.05h/\text{Mpc}$, as indicated by the ΛMDM models. (Some observational data hint on such a possibility, e.g. Miller and Batuski). Then, what is the physical reason of the spectrum feature at $k \sim 0.05h/\text{Mpc}$? Does it have a baryonic nature (the modulation of the power spectrum by the acoustic waves existing in the early Universe in the baryon-radiation plasma)? If so, then the fraction of baryons should
be higher than we think today, $\Omega_b/\Omega_m > 10 - 15\%$. All these questions only stress the importance of further cluster investigations.

5 Conclusions

The experimental data set with a minimal current level of systematic effects can be used to constrain successfully the cosmological parameters of simple dark matter models.

The ‘minimal data set’ includes (i) the LSS constraints based on galaxy cluster observations (the Abell-ACO power spectrum $\Omega$, the density fluctuation amplitude $\sigma_8$ derived from the mass function of nearby and distant clusters, the mean peculiar velocity of galaxies in a sphere of radius $50h^{-1}\text{Mpc}$, the position and amplitude of the first acoustic peak in the angular power spectrum of CMBA $\Omega$), (ii) the small-scale constraints on the amplitude and tilt of the power spectrum obtained from $Ly\alpha$ clouds at $z=2-3$, (iii) the large-scale constraint on the amplitude of the power spectrum obtained from the COBE data $\Omega$, and (iv) the Big Bang nucleosynthesis constraint $\Omega$.

The results of the determination of the cosmological parameters for spatially flat $\Lambda\text{MDM}$ model without cosmic gravity waves by the $\chi^2$ minimization method are listed as follows:

- The $\Lambda\text{MDM}$ model with the best-fit parameters from the first line in Table 1 matches the observational data set best:
  * one sort of massive neutrino is slightly preferable, however the data do not distinguish models with one, two or three massive neutrino species within $1\sigma$ c.l.;
  * the tilt of the power spectrum is consistent with the Harrison-Zel’dovich one;
  * the abundance of matter and cosmological constant is roughly half-to-half,
  * the abundance of hot matter is close to the abundance of baryons and consists $10 - 15\%$ of the total matter abundance,
  * the Hubble constant fits the local SNIa measurements.

- Fixing a low $\Omega_m = 0.3$ the $\Lambda\text{CDM}$ model without hot matter and with high $h>0.7$ matches the observational data set best.

- Fixing a high $\Omega_m = 1$ the standard MDM model with high abundance of hot matter (up to $\Omega_\nu = 0.22$) and extremely low $h \leq 0.5$ matches the observational data set best. The standard CDM/MDM models with $h > 0.5$ are ruled out at very high confidence level, 99.99/95% c.l. respectively.

- Raising fixed Hubble parameter decreases the total matter abundance keeping the production of both factors approximately constant: $\Gamma \equiv \Omega_m h \simeq 0.3$. The same procedure for a fixed low $\Omega_m$ universe ($\Lambda\text{CDM}$) keeps the shape parameter at the level $\Gamma \simeq 0.22$.

- Increasing the number of massive neutrino species raises the abundances of both the hot and total matter, the corresponding correlation between $\Omega_\nu$ and $\Omega_m$ (when the rest parameters are fixed to their best-fit values) is approximated by the equation: $\Omega_\nu \simeq 1.3\Omega_m^2 - 0.44\Omega_m + 0.023$.

- Increasing the tilt of power spectrum raises the value of $\Lambda$-term: $n\sqrt{\Omega_m} \simeq 0.73$.

- For all best-fit models
  * the biasing parameter of rich galaxy clusters remains in the range $b_{\text{Cl}} \simeq 2.2 - 3.3$, the 1$\sigma$ confidence interval is $1.5 \leq b_{\text{Cl}} \leq 3.5$;
  * the power spectra of matter density perturbations do not have percularity at $k \sim 0.05h/\text{Mpc}$ (a better understanding of the cluster power spectrum break or baryonic feature at $k \sim 0.05h/\text{Mpc}$ is required).
• The best-fit models constrained by the 'minimal data set' are
  * consistent with the age of globular clusters, observations of nearby and distant SNIa, evolution of the comoving number density of clusters with redshift;
  * inconsistent with galactic power spectra (a better understanding of the non-linear biasing and different systematics of galaxy catalogues is required).

• The $\Lambda$-term is strongly indicated by the 'minimal data set' based on cluster observations. However, still a low accuracy of the present observational data does not allow
  * to constrain the set of cosmological parameters sufficiently,
  * to discriminate between the $\Lambda$MDM and $\Lambda$CDM models (even at 1$\sigma$ c.l.).

It may well be that the DM nature is more complex than just the $\Lambda$MDM without CGW. The progress in both, the LSS theory and observations based on galaxy clusters helps to solve the DM problem, the key problem of the cosmological model.

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