Spin-orbit coupling (SOC) is a relativistic effect, where an electron moving in an electric field experiences an effective magnetic field in its rest frame. In crystals without inversion symmetry, it lifts the spin degeneracy and leads to many magnetic, spintronic, and topological phenomena and applications. In bulk materials, SOC strength is a constant. Here, we demonstrate SOC and intrinsic spin splitting in atomically thin InSe, which can be modified over a broad range. From quantum oscillations, we establish that the SOC parameter $\alpha$ is thickness dependent; it can be continuously modulated by an out-of-plane electric field, achieving intrinsic spin splitting tunable between 0 and 20 meV. Unexpectedly, $\alpha$ could be enhanced by an order of magnitude in some devices, suggesting that SOC can be further manipulated. Our work highlights the extraordinary tunability of SOC in 2D materials, which can be harnessed for in operando spintronic and topological devices and applications.

**INTRODUCTION**

In a crystal, the twofold degeneracy of spins is protected by the combined inversion symmetry in both space and time. In the well-known Zeeman effect, an external magnetic field breaks the time reversal symmetry (TRS) and splits the spin degeneracy by $g\mu_B B$, where $g$ is the gyromagnetic ratio and $\mu_B$ is Bohr magneton. Alternatively, spin degeneracy can be lifted by spin-orbit coupling (SOC) when spatial inversion symmetry is broken, even in the absence of a TRS-breaking magnetic field. In crystals lacking structural inversion symmetry, the SOC coupling is of the Rashba form, $H_R = \alpha (\mathbf{p} \times \mathbf{\sigma})$, where $\alpha$ is the Rashba parameter, $\mathbf{p}$ is the momentum, and $\mathbf{\sigma}$ is the Pauli spin matrices ($\sigma_x, \sigma_y, \sigma_z$). As a result, the energy band of the crystal is spin-split; within each subband, the charges’ spin is locked to their direction of momentum (Fig. 1A). A large SOC can be used to manipulate spins and generate interesting phenomena (4–6), such as the spin Hall effect, spin–orbit torque, and topological phenomena including the quantum spin Hall effect and quantum anomalous Hall effect.

The advent of two-dimensional (2D) materials provides platforms with unprecedented opportunities for SOC tuning. For instance, sizable SOC can be “endowed” to graphene by proximitization with transition metal dichalcogenides (TMDCs), and intrinsic SOC in 2D materials has been studied by weak-antilocalization measurements (20–22). Here, we exploit the atomically thin sheets of InSe to demonstrate the extraordinary tunability of SOC in 2D materials.

InSe is a layered semiconductor with thickness-dependent bandgaps that range from 1 to 3 eV. Its direct bandgap (except in monolayers), combined with extraordinarily high mobility (23, 24), makes it a very attractive electronic and optoelectronic material. The 2D unit cell of an InSe monolayer is composed of two vertically aligned In atoms, sandwiched between two planes of Se atoms. When projected onto a plane, an InSe monolayer forms a honeycomb lattice, where the metallic and chalcogen atoms occupy the two sublattices, respectively (Fig. 1B). Bulk crystals of InSe are found in several polytypes, including $\gamma$, $\beta$, $\epsilon$, and $\delta$ phases (25). In this study, crystals are grown by the Bridgeman technique and are confirmed by a transmission electron microscope (TEM) to be predominantly $\gamma$ phase with rhombohedral stacking, though stacking faults and nanotwins are rather common (see the Supplementary Materials). The $\gamma$ phase belongs to the space group $R3m$ and is noncentrosymmetric; this lack of inversion symmetry is a key ingredient that allows SOC-induced spin-split bands in the absence of an external magnetic field. Although SOC in InSe has been measured via weak-localization studies on relatively thick flakes (20, 22), the values obtained have relatively large error bars, while the single-gated devices do not allow independent tuning of the Rashba SOC.

Our devices consist of atomically thin InSe sheets with thicknesses ranging from four to 10 layers (Table 1) and sandwiched between hexagonal BN (hBN) layers, with few-layer graphene (FLG) contacts, a silicon back gate, and a metal top gate (Fig. 1C). By varying voltages applied to the top gate $V_{\text{BG}}$ and back gate $V_{\text{BG}}$, we can independently control the charge density $n = \frac{3}{2}(C_{\text{BG}} V_{\text{BG}} + C_{\text{BG}} V_{\text{BG}})$ and out-of-plane electric field $E_z = \frac{C_{\text{BG}} V_{\text{BG}}}{2\varepsilon_0}$, where $C_{\text{BG}}$ and $C_{\text{BG}}$ are capacitance per unit area between the gates and InSe, $\varepsilon$ is the electron charge, and $\varepsilon_0$ is the permittivity of vacuum. We note that the application of $E_z$ is particularly crucial for modulation of Rashba SOC strength, which, depending on the direction of application, can either further break the inversion symmetry or compensate for the built-in asymmetry of the lattice.

**RESULTS AND DISCUSSION**

Figure 1D presents the longitudinal resistance $R_{xx}$ of device D1, which has a thickness of ~6 layers, as a function of back gate voltage and magnetic field $B$. A prominent Landau fan is observed. Shubnikov de Haas (SdH) oscillations start at $B$ as low as 2.5 T, indicating a
quantum mobility exceeding 4000 cm$^2$/Vs, which is the highest value reported to date. At $B > 12$ T, quantized plateaus for filling factor $v < 10$ are observed. To estimate the effective mass of the charge carriers, we extract the amplitude $A$ of the SdH oscillations at $B = 10$ T from the Lifshitz-Kosevich formula.

$$A = \frac{eB}{\pi m^*} \frac{1}{\sinh(\frac{\alpha}{2} T)}$$

The high device mobility enables manifestation of the hallmark signatures of large Rashba SOC in a 2D semiconductor, in which the quadratic band is spin-split by $\Delta_R = 2|\alpha k_F|$ (here, $k_F$ is the Fermi momentum). The different Fermi surface areas of spin-up and spin-down bands give rise to different oscillation frequencies, which interfere to generate the characteristic beating pattern. The Landau level (LL) spectrum is then given by (2, 3, 6)

$$E_N^e = \hbar \omega_c \left[ N + \frac{1}{2} \left( 1 - \frac{g m^*}{2} \right)^2 + N \frac{\Delta_R^2}{E_F^2 \hbar \omega_c} \right], E_0 = \frac{1}{2} \hbar \omega_c$$

Table 1. Device parameters.

| Device | Estimated thickness | $\alpha_0$ (10$^{-11}$ eV m) | $\alpha$ (10$^{-2}$ e nm$^2$) |
|--------|---------------------|-----------------------------|-----------------------------|
| D1     | Six-layer           | 3.5                         | 3.0                         |
| D2     | Four-layer          | 0.6                         | $-1.2$                      |
| D3     | Seven-layer         | 0.2                         | $-1.2$                      |
| D4     | Eight-layer         | 0.15                        | $-1.15$                     |
| D5     | Nine-layer          | 0.08                        | $-1.1$                      |
| D6     | Six-layer           | 0.3                         | 1.1                         |
| D7     | Four-layer          | 0.8                         | 1.3                         |

Fig. 1. Crystal structure, device schematics, and magnetotransport data. (A) Rashba SOC–induced spin splitting of bands. (B) Side and top views of the crystalline structure of γ-InSe. The middle and bottom layers are partially exposed for better visualization (images created using VESTA software ([1])). Inset: Optical image of a device. (C) Schematics of device structure. (D) Landau fan $R_{xx}(V_{sd}, B)$ of device D1 from $B = 0$ to 18 T. (E) SdH oscillations at $B = 10$ T for temperatures ranging from 0.6 to 28 K. Inset: Amplitude of the oscillations as a function of temperature. The line is a fit to the Lifshitz-Kosevich formula.
into minima and vice versa; the transition points move approximately linearly on the $n$-$E_\perp$ plane. In the SdH oscillations regime, the magnetoresistance of the device is related to the LL spectrum by (26)
\[
\rho_{xx} \sim B^2 \sigma_{xx} \sim B^2 \Sigma \left( N \pm \frac{1}{2} \right) e^{-\frac{(E_F-E_\Sigma)}{\Gamma}} \frac{1}{T^2}
\]
where $E_F$ is the Fermi energy and $\Gamma$ is the LL broadening. We model the effect of the electric field by taking
\[
\alpha = |a_0 + \alpha' E_\perp|
\]
where $\alpha$ is the “intrinsic” Rashba parameter, arising from the asymmetry of the intrinsic lattice and the confined potentials, including the different dielectric thicknesses for the gates; $\alpha'$ parametrizes the effectiveness of the electric field at tuning the SOC coupling, which can be positive or negative, depending on the field’s orientation relative to the built-in inversion asymmetry of the lattice. Combining Eqs. 1 and 3, and assuming $\Gamma = 1$ meV, $m^* = 0.14$, we are able to satisfactorily reproduce the data by using $\alpha = 0.6 - 1.2 \ E_\perp$, where $\alpha$ is in units of $10^{-11}$ eV m and $E_\perp$ in V/nm (Fig. 3B). Magnitude of these values agrees with those obtained from density functional theory (DFT) calculations (Fig. 4D) (27, 28). Together, these results underscore the highly tunable nature of the Rashba SOC in a 2D semiconductor, which, by applying an external $E_\perp$, can be enhanced, reduced, and even completely suppressed to zero.

A unique opportunity afforded by the atomically thin 2D membranes is the exploration of SOC in a layer-by-layer fashion. To this end, we fabricate devices on a single piece of InSe flake with adjacent regions that differ by a single atomic layer in thickness (see Supplementary Materials). Figure 3 (C to E) presents data for such a device D3, which hosts regions that are estimated to be seven, eight, and nine layers, respectively. The overall features in the $dR_{xx}/dn(n,E_\perp)$ plots at $B = 6$ T are qualitatively similar, with an important difference: As the thicknesses increase, the transition points shift to lower (more negative) $E_\perp$ values. These patterns can be satisfactorily captured by our simulations, yielding the intrinsic Rashba parameter $a_0 = 0.2 \times 10^{-11}, 0.15 \times 10^{-11}$, and $0.08 \times 10^{-11}$ eV m, respectively, for the regions that are seven, eight, and nine layers thick; $\alpha'$, the effective tunability of the SOC, is extracted to be $-1.2 \times 10^{-11}$, $-1.15 \times 10^{-11}$, and $-1.1 \times 10^{-11}$ eV nm$^2$, respectively. Thus, as the layer number increases, both the intrinsic SOC strength and its scaling with external $E_\perp$ are diminished (27). This trend is opposite to that predicted by theory calculations (28). Such discrepancy is not understood at this point and should stimulate further theoretical and experimental work to explore, for example, variations of hopping parameters with number of layers, variations of intra- and interlayer SOC with energy, and effects of electron interactions and screening. The strength and tunability of the Rashba SOC of different devices are summarized in Fig. 4C.

Last, we observe that some devices appear to be markedly enhanced. Figure 4A presents $dR_{xx}/dn(n,E_\perp)$ at $B = 10$ T for device D1. Notably, instead of a single transition point at a given $n$, several crossing points are visible. Such large number of transitions indicates much higher SOC—we are able to reproduce the patterns by taking $\alpha = 3.5 + 3.0 E_\perp$ (Fig. 4B). Compared to values in the previous plots, $\alpha'$ increases by as much as an order of magnitude, while tunability $\alpha'$ is enhanced by a factor of 3. Such a large SOC strength is unexpected and unlikely to originate from variations such as thicknesses of flake or gate dielectrics. Instead, it suggests a fundamental mechanism at play. One possibility is variations in the interlayer spacing.
c, which, according to DFT calculations, is an extremely effective “knob” to tune the SOC parameter. For instance, increasing c by a mere 1.9% (from 8.43 to 8.6 Å) results in a reduction of α0 by 57% (from 0.89 × 10⁻¹¹ to 0.57 × 10⁻¹¹ eVm) (Fig. 4D). The small variations in interlayer spacing may arise from stacking faults: Although the γ phase is the most dominant phase in our crystals, TEM studies reveal high densities of stacking faults that are generated by dislocation dissociation or by growth, including ones with wrongly stacked monolayers (see figs. S1 and S2). The large electrostatic pressure generated by the displacement fields, which exceeds 20 MPa in our devices, may further compress the interlayer spacing. Another possibility is the nonlinear scaling of α with E⊥ in the presence of stacking faults or twin boundaries. Although further work is required to ascertain the mechanism, these data show that Rashba SOC can be tuned through a much larger range than previously thought possible.

In summary, we observe the hallmarks of large Rashba SOC in few-layer InSe field effect transistor devices, where the unprecedented mobility enables quantitative extraction of the Rashba parameter. The two-dimensionality of the devices enables the SOC strength to be modulated by the layer thickness and by an electric field that breaks or compensates for the inversion symmetry. The possibility of piezo-SOC tuning, which has not been observed to date, warrants further theoretical and experimental investigation. The extraordinary tunability of SOC in 2D materials, as demonstrated here, can be exploited for a variety of phenomenon and devices, such as spin Hall effect, spin-orbit torque, and spin helix with long spin coherence time, with in situ control.

MATERIALS AND METHODS

Single crystals of InSe were synthesized from 6N-pure indium and 6N-pure selenium pellets in a ratio In0.52Se0.48. The starting materials were sealed in a quartz ampule and then vacuumed to 10⁻³ torr. They were subsequently prereacted by gradually heating the ampule to 800°C and kept at this temperature for 96 hours. After the reaction, the ampule was then placed into a radio frequency (RF) furnace where the RF power was gradually increased to raise the temperature up to 800°C. The ampule was then pulled through the hottest zone at a rate of 2 mm/hour.

Bulk InSe crystals are characterized by atomic-resolution high-angle annular dark-field scanning transmission electron microscopy using a probe aberration–corrected JEOL JEM-ARM200cF at...
SUPPLEMENTARY MATERIALS
Supplementary material for this article is available at http://advances.sciencemag.org/cgi/content/full/7/5/eabe2892/DC1

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Layer- and gate-tunable spin-orbit coupling in a high-mobility few-layer semiconductor

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