Reference Design and Comparative Analysis of Model Reference Adaptive Control for Steam Turbine Speed Control

This paper presents the mathematical modeling of the steam turbine unit with the fuzzy controller in an isolated operating condition, especially in nuclear power plants. The water level in the steam generator is one of the main causes for the shutdown of the reactor. This problem has been of immense concern during the past years as the steam generator and governor speed control is a highly nonlinear system showing inverse response dynamics. In the present research a simulink model of turbine with fuzzy controller is designed. The results are compared and analyzed with MRAC design technique to determine better methodological solution for the steam turbine speed control and achieved, time to the adaption effectiveness of 0.3 to 2.5% with and without GDB. Improved set point tracking and control with respect to turbine speed are demonstrated for the cases when governor dead-band is present and absent.

**Keywords** Steam turbine, Governor Dead Band (GDB), Model Reference Adaptive Control (MRAC), Lyapunov rule, Fuzzy Logic Control (FLC).

1. INTRODUCTION

The steam turbines may be used for the applications to drive an electric generator or equipment such as boiler feedwater pumps, process pumps, air compressors, paper mills and refrigeration chillers. The Rankine cycle and thermodynamic principles are the fundamental basis for steam turbines, in conventional power generating stations where water is first pumped to elevated pressure, which is medium to high pressure, depending on the type of turbine unit and then most frequently superheated. For the commercial and industrial applications, the pressurized steam is expanded to lower pressure in a multistage turbine, then exhausted either to a condenser at vacuum conditions or into an intermediate temperature steam turbine, then exhausted either to a condenser at vacuum conditions or into an intermediate temperature steam distribution system and condensate to utilized back. The measured stimulus and response samples of turbine or plants, used for system identification, involve building a mathematical model of dynamic system. System identification is a process of acquiring, formatting, processing and identifying mathematical models based on raw data from the real-world system. System identification of an interacting series process for real-time model predictive control is done and many critical challenging problems are occurring due to the non-linear behaviour in most of the nuclear power plant and chemical industries. Therefore, traditional control techniques are needed for most of the chemical process industries. Conical tanks exhibit non-linear behaviour which is suitable for food process industries, concrete mixing industries, hydrometallurgical industries and waste water treatment industries. [1,2].

The industrial processes are complex in nature. It is difficult to develop a closed loop control model. Also, the human operator is often required to provide online adjustment, which makes the process performance greatly dependent upon the experience of the individual operator. It would be extremely useful if some kind of systematic methodology can be developed for the process control model that is suited to this kind of industrial process. There are some variables in continuous DCS (distributed control system) that suffer from several unexpected disturbances during the operation (noise, parameter variation, model uncertainties), so the human supervision (adjustment) is necessary. If the operator has a little experience, the system may be damaged or operated at lower efficiency. One such system is the control of steam turbine speed using PI controller as the main controller for controlling the process variable. The process is exposed to unexpected conditions and the controller fails to maintain the process variable in a satisfied manner and retuning of the controller becomes necessary. In a nuclear power plant, the water level in the steam generator is one of the main causes that shutdown the reactor, this problem has been of great concern for many years as the steam generator and governor speed control is a highly nonlinear system showing inverse response dynamics. The speed governor dead-band has significant effect on the dynamic performance of load frequency system[3,4].

To cope with the above listed problems, much research has been devoted with various control techniques. Conventional controllers are widely used in industries due to low cost, ease of implementation and tuning. The performance of these conventional controllers has been enhanced by tuning various methods viz Zeigler - Nichol’s and simplex method. Even though, but the conventional PID controllers with fixed gain are...
unable to cope up with the problems discussed above. The use of conventional controllers with artificial intelligence, for control of parameters to get optimal plant performance has been enumerated in this paper[5,6,7,8].

Adaptation of PID controller using techniques like fuzzy logic, the DSP-based laboratory model of Hybrid Fuzzy-PID controller using genetic optimization for high-performance motor drives [9,10] and Neuro fuzzy controller (ANFIS) for speed control of isolated steam turbine had been proposed in the earlier research [11,12] and later on, the neural network is applied to develop the PID controllers to enhance the dynamic characteristics of controller [13]. Research gaps highlights the complete adaptive nature, specific adaptive control techniques, now a days, the adaptive control schemes are making their place where the conventional control system fails with the uncertainty situations, like reference design and analysis of model reference adaptive control (MRAC) for steam turbine speed control loads, inertias and the forces acting on system, changes drastically, possibility of unpredictable and sudden faults, possibility of frequent or unanticipated disturbances.

Among many adaptive control schemes, this paper mainly deals with the combination of model reference adaptive control (MRAC) approach with Lyapunov rule as adjusting mechanism and fuzzy. In MRAC, the output response is forced to track the response of a reference model, irrespective of plant parameter variations, eventhough, the disadvantage of MRAC scheme is time to adapt and leads to oscillations after a certain period, however, fuzzy control methods have a advantage of robustness, which have been demonstrated through the industrial applications [14,15].

Another method, popular in recent years, is based on fuzzy neural network. It is proved that both methods ensure good characteristics, yet the fuzzy neural network requires less control effort. Fuzzy neural networks combine the capability of fuzzy reasoning and the ability of neural networks learning from processes [16,17]. On the other hand, the combination of the fuzzy control base design and the MRAC control causes the reduction of the fuzzy rules significantly. The adaptive fuzzy controller is able to ensure very good dynamical performance of different industrial objects including electrical drives[18,19].

The combination of adaptive and fuzzy control is to work in situations where there is a large uncertainty or unknown variation in plant parameters and structures. A stable speed is useful for the operation of generator under loaded and no load condition. This research identifies the parameters of the steam turbine speed control, compare with the fuzzy logic techniques, MRAC model and to choose the appropriate control method among the two listed techniques with and without GDB(Governor Dead Band).

The paper is divided into five sections. In section 2, steam turbine mathematical model is described. Section 3, model reference adaptive control simulink design is presented. Section 4 design of fuzzy logic controller, section 5 results and discussion of the overall paper is presented. In the next section, the concluding remarks are given to summarize the contribution of the work.

2. MATHEMATICAL MODEL OF THE STEAM TURBINE

Tandem-compound single-reheat steam turbine assembly is composed of four stages in line on the same shaft with several casings. The superheated steam enters the high-pressure stage (HP) where it expands through the small diameter rotor blades before exiting and being returned to the boiler. In the boiler the steam is superheated and is directed to the intermediate pressure stage (IP). Here, it expands through larger diameter rotor blades exiting to the low-pressure turbines. In the final stage there are two identical sets of low-pressure turbines (Dual LP), the exiting steam from the IP turbine is divided equally between the two turbines passing through quite large diameter rotors and blades along with that main inlet stop valves (MSV), main inlet control (governor) valves (CV), reheater stop valves (RSV), reheater intercept valves (IV) shown in figure 1[3]. The steam turbine mathematical model has two parts: first, simplified transfer function of a linear steam turbine which associates with the change in mechanical power $\Delta P_M$, the changes in steam valve position $\Delta P_{GV}$ and second, of turbine-governor model, considering nonlinear characteristics.

Figure 1. Tandem compound single reheat steam turbine

2.1 Transfer Function of a Linear Single reheat Steam Turbine

The model for a single reheat tandem-compound steam turbine shown in figure 2 is presented in this paper. Large steam turbines are used in fossil fuel power plants, fossil fuel plants typically burns coal to heat a boiler that produces high boiler that produces high-temperature, high-pressure steam, which is passed through the turbine.

Figure 2. Single Reheat tandem-compound steam turbine model

The actual transfer function for steam turbine can be considered as

$$G_{HP} = \frac{1}{1 + sT_{HP}}$$

$$G_{MP} = \frac{1}{1 + sT_{MP}}$$
\[ G_{IP}(s) = \frac{0.3}{0.5s + 1} \]  
\[ G_{GV}(s) = \frac{0.4}{0.25s + 1} \]  
\[ G_{LP}(s) = \frac{0.3}{0.1s + 1} \]  

Expression (4) indicates the fraction of power generated in the HP section, medium section and the low section, and its summation should be equal to 1. Substituting the values for the parameters from the table 1.

\[ F_{HP} + F_{MP} + F_{LP} = 1 \]  

The overall transfer function for the system, describes the mechanical power with the change in steam valve position, where \( F_{IP} = F_{HP} \). Assume \( T_{CO} \) is negligible compared to \( T_{RH} \) and \( T_{CH} \), then the CV characteristics is linear.

Table 1. Steam turbine parameter list [12]

| Parameter | Unit | Description | Default | Min | Max |
|-----------|------|-------------|---------|-----|-----|
| \( F_{IP} \) | p.u | High pressure turbine power fraction | 0.3 | -2 | 1 |
| \( F_{MP} \) | p.u | Medium pressure turbine power fraction | 0.4 | 0 | 3 |
| \( F_{LP} \) | p.u | Low pressure turbine power fraction | 0.3 | 0 | 1 |
| \( T_{RH} \) | Sec | Reheat time constant | 0.5 | 0.01 | 20 |
| \( T_{HP} \) | Sec | Steam Chest time constant | 0.25 | 0 | 1 |
| \( T_{LP} \) | Sec | Crossover piping time constant | 0.1 | 0.01 | 1 |
| \( T_{SM} \) | Sec | Valve positioner time constant | 0.5 | 0.04 | 1 |

Where \( \Delta P_M \) is change in mechanical power, \( \Delta P_{GOV} \) is change in valve position.

\[ \frac{\Delta P_M(s)}{\Delta P_{GOV}(s)} = \frac{1 + sT_{MS}T_{rs}}{1 + sT_{GOV}} \]  

The actual transfer function for steam turbine is obtained after the substitution of values from table 1 and expressions 1, 2 and 3.

\[ \frac{\Delta P_M(s)}{\Delta P_{GOV}(s)} = \frac{1 + (0.3)(0.5)s}{1 + (0.5s)(0.25s)} = \frac{1.2s + 8}{s^2 + 6s + 8} \]  

2.2 Typical design model of steam turbine control

A typical governor model for steam turbines has two main sections, the governor and steam control valve, whose output is effective control valve area in response to speed deviation of the machine and a section modeling the turbine, whose input is steam flow and output is mechanical power applied to the rotor. In the block diagram (figure 3), where \( G_g(s) \) is a governor transfer function, \( G_{sr}(s) \) is a speed relay transfer function, \( G_{sm}(s) \) is a servo motor transfer function, \( G_P(s) \) is a system/plant transfer function.

\[ \omega_{ref} = \frac{1}{T_{gs} + 1} \]  

Here, \( T_g \) and \( T_{rs} \) are governor and speed relay time constants respectively. Transfer function of mechanical power to steam valve position is considered as

\[ \frac{\Delta P(s)}{\Delta \omega_{ref}(s)} = \frac{1}{(1 + sT_{gs})(1 + T_{ch})} \]  

The overall linear transfer function of a system is obtained as below

\[ \omega_{ref} = \frac{1.5S}{S^2 + 112S^2 + 1180S^2 + 4752S^2 + 8320S + 5333.3} \]
2.3 Design model of turbine governor considering the nonlinear characteristics

In fact, due to the factors like machinery manufacturing, the governor has some nonlinear characteristics such as the rate-limit characteristic, amplitude-limit characteristic, dead band characteristic, clearance nonlinearity characteristic, etc. Therefore, describing function approach is used to incorporate the GDB non-linearity which may be expressed by,

\[ Y = F(x, \dot{x}) \]  

(14)

To solve this non-linear problem by DF (Describing Function) approach, it is necessary to make the basic assumption that the variable \( x \), appearing in the non-linear function \( F(x, \dot{x}) \) is sufficiently close to a sinusoidal oscillation and is given as

\[ x = A \sin(\omega_0 t) \]  

(15)

As the variable function is complex and periodic function of time, it can be developed in a Fourier series as

\[ F(x, \dot{x}) = F^0 + N1x + \frac{N2}{\omega_0} \frac{\partial x}{\partial \omega} + \ldots \]  

(16)

After neglecting the higher order terms (assuming low pass filter) and backlash nonlinearity is symmetrical about the origin, \( F^0 \) is zero so the expression (18) will be as follows

\[ F(x, \dot{x}) = N1x + \frac{N2}{\omega_0} \frac{\partial x}{\partial \omega} \]  

(17)

The Fourier co-efficient are derived as \( N1 = 0.8 \) and \( N2 = -0.2 \) [8]

\[ F(x, \dot{x}) = 0.8x - \frac{0.2}{\omega_0} \dot{x} \]  

(18)

The governor transfer function with linearized dead-band is derived as Equation (19), when the governor transfer function is

\[ G_g(s) = \frac{1}{T_{gr} + 1} \]  

(19)

\[ G_g(s) = \frac{N1 + N2}{T_{gr} + 1} \]

Substituting the values of \( N1 \) and \( N2 \) in expression (19) and rearranged \( G_g(s) \) as

\[ G_g(s) = \frac{0.8 - 0.064}{0.5s + 1} \]  

(20)

2.4 Stability analysis of a system using Kharitonov Stability Checker

Kharitonov polynomials are associated with the interval polynomials \( p(a) \), are expressed as four fixed Kharitonov polynomials.

\[ p^+(s) = a_1^s + a_2^s + a_3^s + a_4^s + \ldots \]  

\[ p^-(s) = a_1^- + a_2^- + a_3^- + a_4^- + \ldots \]  

\[ p^0(s) = a_1^0 + a_2^0 + a_3^0 + a_4^0 + \ldots \]  

\[ p^-0(s) = a_1^- + a_2^- + a_3^- + a_4^- + \ldots \]  

Stability analysis steps are narrated as 1. Formulating the interval system model (figure 4) 2. Obtaining the four Kharitonov Polynomials 3. Applying Routh-Hurwitz Criterion to the four polynomials 4. If all the four polynomials are stable, without any sign change in the first column of the R-H Table, then the given interval system is stable[13].

\[ \frac{\Delta \text{Uc}(s)}{\Delta \text{Pref}(s)} = \frac{0.8 - 0.064}{0.5s + 1} \]  

(21)

With unity feedback the expression 21 becomes,

\[ \frac{\Delta \text{Uc}(s)}{\Delta \text{Pref}(s)} = \frac{0.8 - 0.064}{0.436s + 1.8} \]  

(22)

The speed relay is represented as an integrator with time constant \( T_{sr} \) and direct feedback as

\[ \frac{\Delta \text{Ps}(s)}{\Delta \text{Uc}(s)} = \frac{1}{0.01s + 1} \]  

(23)

2.5 Design of governor transfer function with DB

The speed governor produces a position which is assumed to be a linear, instantaneous indication of speed and is represented by a gain \( K \) which is reciprocal of regulation or drop. It represents a composite load and speed reference and is assumed constant over the interval of a stability study.

Governor with dead-band is considered as,

\[ \frac{\Delta \text{Ps}(s)+ \Delta \text{Pref}(s)}{\Delta \text{Uc}(s)} = \frac{0.8 - 0.064}{0.5s + 1} \]  

(24)

2.6 Design of servomotor transfer function

The servomotor is represented by an integrator with time constant \( T_{sm} \) and direct feedback, the valves moves and is physically large, particularly on large units. Rate limiting of the servomotor may occur for large and rapid speed deviation, rate limits are shown at the input to the integrator. Position limits are also indicated and may correspond to wide-open valves or the setting of a load limiter [17]. From expression (10) of change in valve position to change in speed transfer function is obtained as in expression (24).

\[ \frac{\Delta \text{Ps}(s)+ \Delta \text{Pref}(s)}{\Delta \text{Uc}(s)} = \frac{0.8 - 0.064}{0.5s + 1} \]  

(24)
The vector-matrix form of the speed governing system is expressed as follows from figure 5.

\[
\frac{d}{dt} \begin{bmatrix} \Delta P_{GV} \\ \Delta P_{sr} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta P_{GV} \\ \Delta P_{sr} \end{bmatrix} + \begin{bmatrix} \frac{1}{T_{sm}} \\ \frac{1}{T_{sr}} \end{bmatrix} \Delta \omega_{ref} + \begin{bmatrix} \frac{1}{T_{sm}} \\ \frac{1}{T_{sr}} \end{bmatrix} \Delta \omega
\]

(25)

where Kg is speed droop gain (state feedback gain) and substituting the numerical values for T_{sm}, T_{sr} and Kg, the alternative speed governing vector matrix is expressed (27).

\[
\frac{d}{dt} \begin{bmatrix} \Delta P_{GV} \\ \Delta P_{sr} \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} \Delta P_{GV} \\ \Delta P_{sr} \end{bmatrix} + \begin{bmatrix} \frac{1}{T_{sm}} \\ \frac{1}{T_{sr}} \end{bmatrix} \Delta \omega_{ref} + \begin{bmatrix} \frac{1}{T_{sm}} \\ \frac{1}{T_{sr}} \end{bmatrix} \Delta \omega
\]

(26)

Since it is closed loop, the overall transfer function is obtained as

\[
G(s) = \frac{G(s)G_{os}(s)G_{om}(s)}{1 + KG(s)G_{os}(s)G_{om}(s)} \]

(28)

Substituting the all transfer functions in expression 28 and expression 29 is obtained,

\[
G(s) = \frac{1}{1 + \frac{1}{1 + F_{tr}T_{sm}T_{sr}} + F_{tr}T_{sm}T_{sr}} \frac{1}{1 + \frac{1}{1 + F_{tr}T_{sm}T_{sr}} + F_{tr}T_{sm}T_{sr}} + \frac{1}{1 + \frac{1}{1 + F_{tr}T_{sm}T_{sr}} + F_{tr}T_{sm}T_{sr}}
\]

(29)

After rearranging and Substituting the values, where K=1, where K=1/R.

\[
G(s) = \frac{1}{1 + \frac{1}{1 + F_{tr}T_{sm}T_{sr}} + F_{tr}T_{sm}T_{sr}}
\]

(30)

Using the stability analysis for the above expression, the interval system model is formulated as,

\[
\begin{align*}
&\Delta P_{sa} = \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} \\
&\Delta P_{sa} = \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa}
\end{align*}
\]

(31)

Based on the expression (29) of G(s), the complete model for the governor- turbine is obtained as below in figure 6.

\[
\begin{align*}
&\Delta P_{sa} = \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} \\
&\Delta P_{sa} = \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa} + \Delta P_{sa}
\end{align*}
\]

(32)

Then the Kharitonov polynomials is derived as below,

\[
\begin{align*}
&P_{s+}(s,a) = 16001 + 14792s + 6803s^2 + 1431s^3 + 116s^4 + 2s^5 \\
&P_{s+}(s,a) = 16001 + 14792s + 6803s^2 + 1431s^3 + 116s^4 + 2s^5
\end{align*}
\]

(33)

Based on the expression (29) of G(s), the complete model for the governor- turbine is obtained as below in figure 6.

3. PROPOSED MRAC DESIGN FOR STEAM TURBINE

In a general approach its common to specify the ideal response of the adaptive control system to external com-
mands, which reflects the performance specifications in control tasks. The ideal control specified by the reference model should be achievable for the adaptive control system. In this work the critically damped second order system is taken as the reference model and is usually parameterized by a number of adjustable parameters. Two parameters $\theta_1$ and $\theta_2$ are used to define a linear control law, adaptive controller design normally requires linear parameterization in order to obtain adaptation mechanism with guaranteed stability and tracking convergence. The values of these control parameters are mainly dependent on adaptation gain which in turn changes the control algorithm. Lyapunov method is used for constructing the controller. A generalized structure of MRAC with two loops: an inner loop (or regulator loop) that is an ordinary control loop consisting of the plant and the regulator is shown in figure 7 [20-22].

Figure 7. Generalised Structure of MRAC

3.1 Mathematical Modelling of steam turbine with MRAC

A second order underdamped system with large settling time, very high maximum overshoot and with intolerable dynamic error is taken as a plant. The objective is to improve the performance of this system by using adaptive control scheme. For this purpose, a critically damped system is taken as the reference model. The following second order system of steam turbine plant is used from expression (27)[23-25].

$$G(s) = \frac{1.2s + 8}{s^2 + 6s + 8}$$

The Controller output is expressed as,

$$U = \theta_1 U_C(s) - \theta_2 y(s)$$  \hspace{1cm} (32)

Assume the plant transfer function as,

$$y = \frac{1}{\alpha^3}(\alpha^1 U + \alpha^2 U c - \alpha^4 y - \alpha^5 y)$$  \hspace{1cm} (33)

And consider the model transfer function as,

$$G(s) = \frac{64}{s^2 + 16s + 64} = \frac{ym(s)}{U(s)}$$  \hspace{1cm} (34)

Then plant model follower is expressed as,

$$\dot{y}_m = \ddot{y}$$

Assuming the zero initial conditions, the controller output is obtained as,

$$64U_C - 16\ddot{y} - 64\dot{y} = \frac{1}{\alpha^3}(\alpha^1 U + \alpha^2 U c - \alpha^4 y - \alpha^5 y)$$

Rearranging the above expression, expression 35 is achieved,

$$64\alpha_3 U - 16\alpha_3 y - 64\alpha_3 y = \alpha_1 U + \alpha_2 U - \alpha_4 y - \alpha_5 y$$  \hspace{1cm} (35)

Initial values of controller parameters $\theta_1$, $\theta_2$ and error parameter $e$ is calculated as below,

$$\theta_1 = \frac{64\alpha_3}{\alpha_2}$$  \hspace{1cm} (36)

$$\theta_2 = \frac{\alpha_5 - 64\alpha_3}{\alpha_2}, e = y(s) - y_m(s)$$  \hspace{1cm} (37)

For the stability analysis, the Lyapunov function $V$ is defined as,

$$V(\epsilon, \theta, \theta_2) = \frac{1}{2}(\epsilon^2 + \frac{1}{\alpha^2}((\alpha^2\theta_2 + 6\alpha_3 - \alpha_5)^2 + \frac{1}{\alpha^2}(\alpha^2\theta_1 + 6\alpha_3)^2)$$  \hspace{1cm} (38)

Time derivative of Lyapunov function $V$ is expressed as,

$$\frac{dV}{dt} = -\alpha^2 e^2 + \frac{1}{\alpha^2}((\alpha^2\theta_2 + 6\alpha_3 - \alpha_5)^2 + \frac{1}{\alpha^2}(\alpha^2\theta_1 + 6\alpha_3)^2) + \gamma U$$  \hspace{1cm} (39)

Therefore, the updated controller parameters are obtained (adjustment rules) as below,

$$\frac{d\theta_1}{dt} = -\gamma U c e$$  \hspace{1cm} (40)

$$\frac{d\theta_2}{dt} = \gamma U e$$  \hspace{1cm} (41)

3.2 With/without GDB MRAC control design using SIMULINK

Refer to the parameters listed in table 2, the entire simulation design for the turbine model is carried out. The figure 8 and figure 9 shows the Simulink designs of MRAC with and without GDB respectively.

Table 2. Designed Simulation Parameters Values

| Parameter                  | Symbol | Unit | Min  | Max  |
|----------------------------|--------|------|------|------|
| Dead Zone Ranges           |        | p.u  | -2.5 | 2.5  |
| Saturation ranges          |        | p.u  | -0.5 | 0.5  |
| Position limiter           |        | p.u  | 0    | 1    |
| Step input                 | Pref   | Sec  | 0    | 1    |
| Adaptation gain            | $\gamma$ | p.u  | 0.04 | 1    |
| Speed drop gain (state feedback gain) | $K_G$ | p.u  | 0.01 | 0.05 |
| Step load change           | Pl     | p.u  | 0.01 | 0.05 |
| Gain1                      |        |      | 0    | -6   |
| Gain                        |        |      | 0    | 5    |
| Gain4                       |        |      | 0    | 1    |
| Gain6                       |        |      | 0    | 6    |
| Time Function              |        |      | 0    | 2    |
| Speed Droop=1/R            |        |      | 0    | 1    |

In MRAC GDB design of figure 8, the dead zone and governor have common unity feedback, which is
used for error compensation and for the reference input of speed/power a frequency amplifier is used for applying the large step input. The simulation is carried out by changing the gain parameter of $\theta_1$ and $\theta_2$ and the servomotor is represented by an integrator with time constant $t_{un}$. Direct feedback and controls the valves. Position limiter is the heightened control parameter and rate limiter has been discussed earlier with wide-open valves or setting of a load limiter.

**Figure 8. Simulink model of MRAC with GDB**

**Figure 9. Simulink model of MRAC without GDB**

**Figure 10. Fuzzy Logic Control system for steam turbine**
4. PROPOSED FUZZY LOGIC CONTROLLER DESIGN USING SIMULINK

In the proposed design the input to the fuzzy logic controller is the error between the rotor inertial speed and reference speed. The rotor inertial speed \( \Delta \omega_r \) is multiplied with speed droop \( 1/R \) and subtracted from reference speed \( \Delta \omega_{ref} \) to yield the error. The error is fed to the fuzzy logic controller, shown in figure 10. The proposed model shown in figure 11. The design parameter is considered as the same from table2 used for the MRAC design [26].

4.1 Fuzzy Membership functions for speed change error (e)

In this proposed fuzzy controller design, triangular fuzzy membership function is chosen to control the steam turbine speed control, two inputs and one output variables are proposed. It maps the values of fuzzy variables in a certain region to the degree of membership \( \mu \) between 0 and 1. Input variable-1 is speed change error and input variable-2 is rate of change speed error. Output variable is change in valve position, the structure of fuzzy logic controller is mamdani type.

Table 3. Fuzzy set and MFs for speed change error(e)

| Fuzzy Set | Range of MFs | Membership function chosen |
|-----------|--------------|----------------------------|
| Low       | -50 to 0 OR 0 to 50 | Triangular                 |
| Normal/medium | 0 to 50 OR 50 to 100 | Triangular                 |
| High      | 50 to 100 OR 100 to 150 | Triangular                 |

4.2 Fuzzy Membership functions for rate of change of speed error (de/dt)

Rate of change of Speed error is second variable inputs which is fuzzified into two triangular membership functions and scaled in the range from -30 to 30, as shown in figure 13 and Table 4. The two MF of rate of change of speed are Negative and Positive. The value of -30 indicates that lowest rate of change of speed and the value of 30 indicates that highest rate of change of speed. Triangular type of membership function produced good result for the ranges of the variables considered.

Table 4.Fuzzy set and MFs for input rate of change in speed error(de/dt)

| Fuzzy Set | Range of MFs | Membership function chosen |
|-----------|--------------|----------------------------|
| Negative  | -30 to -10 OR -10 to 10 | Triangular                 |
| Positive  | -10 to 10 OR 10 to 30 | Triangular                 |

4.3 Fuzzy set and Membership Function for valve position (output variable)

The change in valve position is the output fuzzy variable which is evaluated for each bus by considering speed change error and rate of change of speed as input variables to the fuzzy expert system using a set of rules,
which are developed from qualitative descriptions. These rules are summarized in the fuzzy decision rule given in table 6, change in valve position is a fuzzy variable having five triangular membership functions and scaled in the range from -25 to 125, as shown in figure 14 and Table 5. The five membership functions of change in valve position are Close Fast (CF), Close Slow (CS), No change (NC), Open slow (OS) and Open Fast (OF). The minimum value of change in valve position indicates the highest speed of the steam turbine.

The range for the MF was chosen based on the valve angle position opening percentage 100%, 75%, 50%, 25% and 0% to show respectively, fully opened, almost fully opened, half opened, close slow and total closed position of valve.

Table 5. Fuzzy set and MFs for valve position (output variable)

| Fuzzy set       | Range of MFs         | Membership Function chosen |
|-----------------|----------------------|-----------------------------|
| Close fast      | -25 to 0 OR 0 to 25  | Triangular                  |
| Close slow      | 0 to 25 OR 25 to 50  | Triangular                  |
| No change       | 25 to 50 OR 50 to 75 | Triangular                  |
| Open slow       | 50 to 75 OR 75 to 100| Triangular                  |
| Open fast       | 75 to 100 OR 100 to 125| Triangular                |

Figure 14. Membership Function of valve position (the output variable)

4.4 Fuzzy Set Rule Base

The design of the fuzzy controller essentially consists of choosing a set of rules (“rule base”), where each rule is based upon the knowledge that one has about the system. The following set of rules are designed which equivalently shown in table 6 for the proposed design [27,28].

Table 6. Selection of Fuzzy Set Rule Base

| SL.No. | Fuzzy Set Rule                                                                 | Without any control (With GDB) | With MRAC (Without GDB) |
|--------|--------------------------------------------------------------------------------|-------------------------------|-------------------------|
| 1      | If (Speed_change is Low) then (valve_position is Open_fast) (1)                  | 2.86 32.23 18.83 18.57 18.34 18.21 | γ = 0.1 γ = 0.2 γ = 2 γ = 5 |
| 2      | If (Speed_change is Normal) then (valve_position is No_change) (1)               | 14.37 0.505 0.504 0.504 0.504 0.504 |                          |
| 3      | If (Speed_change is High) then (valve_position is Close_fast) (1)               | 3.23 1.97 1.875 1.92 1.94 1.97   |                          |
| 4      | If (Speed_change is Normal) and (Rate is Positive) then (valve_position is Close_slow) (1) | 1.43 2.14 1.39 1.34 1.32 1.318 |                          |
| 5      | If (Speed_change is Normal) and (Rate is Negative) then (valve_position is Open_slow) (1) | -0.035 -0.063 -0.59 -2.2 0.2 0.37 |                          |

5. SIMULATION RESULTS

5.1 MRAC with/without GDB Control Design

Simulation results are obtained and analysis is conducted using the developed model. Basic characteristics and the effects on the stability were established. It can be observed that the characteristic of the plant with GDB is oscillatory with high value of overshoot and undershoot whereas the characteristic of the reference model is smooth without any oscillation. There is a large dynamic error between these two methods and that error has to be reduced to zero by using MRAC scheme. The adaptation gain (γ) is varied with a reference range from (0.1 to 5), it changes the values of control parameters 01 and 02 respectively. These values of control parameters are used to improve the plant parameters.

Figure 15.(a) Comparison between Reference speed, actual speed versus time for the system without GDB and Controller. (b) Comparison between Reference speed, actual speed versus time for the system with GDB and without controller

Table 7. Time Response Specifications With and without GDB For Different Adaptation Gain (From Figure 2, 3, 4 And 5)

| Parameter          | Without any control (With GDB) | With MRAC (Without GDB) |
|--------------------|--------------------------------|-------------------------|
| Peak time (sec)    | 2.86 32.23 18.83 18.57 18.34 18.21 | γ = 0.1 γ = 0.2 γ = 2 γ = 5 |
| Maximum overshoot %| 14.37 0.505 0.504 0.504 0.504 0.504 |                          |
| Undershoot %       | 3.23 1.97 1.875 1.92 1.94 1.97 |                          |
| Rise time (sec)    | 1.43 2.14 1.39 1.34 1.32 1.318 |                          |
| With MRAC With GDB | -0.035 -0.063 -0.59 -2.2 0.2 0.37 | 1.85 4.33 |

With GDB

| γ = 0.1 | γ = 0.2 | γ = 2 | γ = 5 |
|---------|---------|-------|-------|
| 19.66 | 19.47 | 19.2 | 19.24 |
| 0.505 | 0.505 | 0.505 | 0.505 |
| 1.913 | 1.99 | 1.86 | 1.96 |
| 1.972 | 1.967 | 1.965 | 1.964 |
| -0.044 | -0.089 | -0.88 | -2.2 |
| 0.2 | 0.37 | 3.114 | 7.53 |
Figures 15-18 shows the output characteristics (responses curve) for the system with GDB and without GDB under MRAC with error curve.

Figure 15(a) shows the Comparison between Reference speed, actual speed versus time for the system without GDB and Controller. Figure 15 (b) shows the Comparison between Reference speed, actual speed versus time for the system with GDB and without controller. Figure 16 (a) shows the tracking error for adaptation gain values $\gamma=0.2$, $\gamma=0.5$, Theta 2 without GDB and figure 16(b) shows the tracking error for adaptation gain values $\gamma=0.2$, $\gamma=0.5$, theta1 without GDB.

![Figure 16(a)](image1.png)

![Figure 16(b)](image2.png)

Figure 16. (a) Tracking error for adaptation gain values $\gamma=0.2$, $\gamma=0.5$, Theta 2 without GDB (b) Tracking error for adaptation gain values $\gamma=0.2$, $\gamma=0.5$, Theta1 without GDB.

Figure 17 (a) shows the Comparison between Reference speed, actual speed versus time for gain values $\gamma=0.1$, $\gamma=0.5$ MRAS with GDB and Figure 17 (b) shows error for the MRAS with GDB for varying adaptation gain values $\gamma=0.1$, $\gamma=0.5$.

![Figure 17(a)](image3.png)

![Figure 17(b)](image4.png)

Figure 18 (a) Comparison between Reference speed, actual speed versus time for gain values $\gamma=0.1$, $\gamma=0.5$ MRAS without GDB (b) Error for the MRAS without GDB for varying adaptation gain values $\gamma=0.1$, $\gamma=0.5$.

Table 8 Time to reach first peak with and without GDB

| Step Load Change in (p.u) | Fuzzy Logic Controller with GDB in sec | MRAC with GDB in sec | % Improvement With GDB |
|---------------------------|---------------------------------------|----------------------|------------------------|
| 0.01                      | 19.000                                | 17.86                | 1.5                    |
| 0.015                     | 19.006                                | 17.91                | 1.68                   |
| 0.02                      | 19.070                                | 17.902               | 0.33                   |
| 0.05                      | 19.032                                | 17.93                | 0.74                   |

Table 7 shows the comparative results of MRAC and without controller, simulation has been carried out for different load changes. Figure 19 and figure 20 depicted the result analysis with and without considering the GDB, for step load changes of $\Delta P_l$ equal to 0.01 and 0.05 p.u for both fuzzy logic controller and MRAS respectively. The peak time of the system frequency is not found to be satisfactory with MRAS controller, but with that of fuzzy logic Controller the peak time is improved significantly. In the absence of GDB, it is evident, from figures 18, 19 and table 7, that first peak is significantly reduced to 35% of the MRAS controller performance. It is clearly shown that the by considering GDB 1st peak is greatly reduced to 30% of the MRAS controller.

5.2 Fuzzy Logic Controller design

Table 7 shows the comparative results of MRAC and without controller, simulation has been carried out for different load changes. Figure 19 and figure 20 depicted the result analysis with and without considering the GDB, for step load changes of $\Delta P_l$ equal to 0.01 and 0.05 p.u for both fuzzy logic controller and MRAS respectively. The peak time of the system frequency is not found to be satisfactory with MRAS controller, but with that of fuzzy logic Controller the peak time is improved significantly. In the absence of GDB, it is evident, from figures 18, 19 and table 7, that first peak is significantly reduced to 35% of the MRAS controller performance. It is clearly shown that the by considering GDB 1st peak is greatly reduced to 30% of the MRAS controller.
The comparative result of fuzzy logic Controller and MRAS controller with and without GDB is given in table 8, from the tabulated results, it is evident that the fuzzy logic controller performance is better over the MRAS controller.

5.3 Comparative analysis of MRAC and FLC

The comparative results analysis is made with reference MRAC and FL controllers shown in figure 21 and 22. It infer from these results that the steam turbine speed control is more responsive to FL controller than to MRAC for both when GDB is present and absent. It attribute this to the simplicity and quick adaptability of FL controller as compared with MRAC.

6. CONCLUSION

A Fuzzy and MRAS Controllers are proposed to be analysed comparatively. A detailed comparison between these techniques has been carried out. The simulation has demonstrated that without any control under inclusion of GDB and without GDB, with both conditions the plant performance is very poor with very high values of overshoot and undershoot. However, the application of MRAC by using Lyapunov stability theory reduces the value of overshoot and undershoot specially for plant without GDB.

The increment in adaptation gain both the peak time and rise time for the case with and without GDB decreases. Also, the control parameters vary in the direction to improve system performance with the increment in adaptation gain. But beyond the chosen range of adap-
tation gain \((0.1 \leq \gamma \leq 5)\), the system performance is very poor for both the case without any controller and MRAC. The system may even become unstable for the wrong choice of adaptation gain. Therefore, it is shown that for suitable values of adaptation gain, the Lyapunov stability theory makes the plant output as close as possible to reference model in MRAC comparing to the case of without any controller. But comparing the MRAC with the fuzzy logic controller using step input, the time to reach first peak with GDB is 19.00s and without GDB for fuzzy logic is 17.86s and 19.29s with and 18.21s without GDB for MRAC. This can be 1.5% with GDB and 1.92% without GDB improvement between fuzzy and MRAC, so based on the findings presented in the earlier discussion, proposed fuzzy logic controller response is more satisfactory.

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NOMENCLATURE

| Symbol | Description |
|--------|-------------|
| $F_{hp}$ | High pressure turbine power fraction |
| $F_{mp}$ | Medium pressure turbine power fraction |
| $F_{lp}$ | Low pressure turbine power fraction |
| $T_{RLH}$ | Reheat time constant |
| $T_{HP}$ | Steam Chest time constant |
| $T_{LP}$ | Crossover piping time constant |
| $T_{sm}$ | Valve positioner time constant |
| $T_{g}$ | Governor time constant |
| $K_{g}$ | Speed drop gain (state feedback gain) |
| $T_{g}$ | Speed Relay time constant |
| $G_{HP}$ | High pressure transfer function |
| $G_{MP}$ | Medium pressure transfer function |
| $G_{LP}$ | Low pressure transfer function |
| $\Delta P_{GF}$ | Change in Steam valve position |
| $\Delta P_{m}$ | Change in mechanical power |
| $\theta_1$, $\theta_2$ | Controller parameters |

РЕФЕРЕНТНИ ДИЗАЈН И КОМПАРАТИВНА АНАЛИЗА АДАПТИВНОГ УПРАВЉАЊА НА БАЗИ РЕФЕРЕНТНОГ МОДЕЛА КОД УПРАВЉАЊА БРЗИНОМ ПАРНЕ ТУРБИНЕ

А. Феjo, А.Р. Телкар, Ц. Бхаратираца, Ј. Аделаjo

Приказује се математичко моделирање склопа парне турбине са фази контролером у изложеним радним условима, нарочито у нуклеарним електранама. Ниво воде у парном генератору је један од главних узрока искушења реактора. Овај проблем је послећих година постао актуелан јер парни генератор и контрола брзине управљања представљају нелинеарни систем који показује инверзну динамику одзива. Дизајниран је SIMULINK модел турбине са фази контролером. Резултати су упоређени и анализирани техником MRAC дизајна да би се нашло боље методолошко решение контроле брзине код парне турбине и постигло ефективно време адаптације од 0,3 до 2,5% са и без GDB. Побољшање праћења задате тачке и контрола брзине турбине по времену приказана је за случајеве у присуству и одсуству промене опсега улазне величине.