Neural Networks for Interferences Suppression in DS/CDMA with Rayleigh Fading Channel and Power Control Error

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Abstract: The exponential chip weighting waveforms have been designed with the purpose of multiple access interferences (MAI) rejection based on the concept that the optimum despreading sequence in reference emphasizes the transitions in the received spreading signal of interest. The despreading sequence weighted by exponential chip waveforms was determined by only one parameter. The objective of this study, was to introduce neural networks (NN) to facilitate the computing of the bit error rate (BER) performance of a direct sequence code division multiple access (DS/CDMA) system over a Rayleigh multipath fading with power control error, for both coherent and noncoherent receivers, by producing the despreading sequences weighted (WDS) by exponential chip weighting waveforms. Numerical results show that the parameter values of the exponential chip weighting waveforms produced by the proposed network are nearly optimal and satisfactory in viewpoint of the achieved bit error rate (BER) performance.

Key words: Multiple access interferences, code division multiple access, weighted despreading sequences, neural networks, rake receiver, bit error rate

INTRODUCTION

The major limitation in the bit error rate (BER) and system performance and hence capacity, is due to multipath fading, (MAI) and imperfect power control. With the objective of MAI rejection, most of works had been made on CDMA performance in presence of multipath fading and are based on the fact that power control is perfect\(^{[1-3]}\), which is not really possible in practice.

In a previous work\(^{[4]}\), the BER performance of a DS/CDMA system was analyzed with power control error over a multipath Rayleigh fading channel using both coherent and noncoherent receptions, the receivers under consideration employ the despreading sequences weighted (WDS) by adjustable exponential chip waveforms optimized for MAI rejection. The chip weighting waveforms employed are determined by only one parameter that leads to easy tuning of the waveforms in practice to achieve the best performance.

It is useful to note that the derived closed-form solutions, which enable to calculate de BER in\(^{[4]}\), require perfect definition of the spreading sequences for the signals of all users. Also, a number of computational efforts are needed to define the parameters of each spreading sequence.

In this work, Our objective is to reduce the computational intensity and shorten the process time to obtain optimal values of the parameter by using the learning ability and the high-speed computational capacity features of neural networks. Throughout the study, we have assumed that a receiver in the DS/CDMA system is perfectly capable of regenerating the reference spreading codes corresponding to each of the users’ transmissions.

System description

Transmitter model: From the transmitter model presented in\(^{[4]}\) which suppose that there are K users sharing the channel in a DS/CDMA system, the transmitted signal by the \(kth\) user is given by:
\[ S_k(t) = \sqrt{2}P_k b_k(t) a_k(t) \cos(\omega_0 t + \theta_k) \]  

(1)

Where \( P \) and \( \omega_0 \), common to all users, are the transmitted power and the carrier frequency, respectively and \( \theta_k \) is the phase introduced by the \( k \)th modulator. The parameter \( G_k \) represents the power control error for the \( k \)th user and is modeled as a random variable uniformly distributed in \([1 - \epsilon_m, 1 + \epsilon_m]\) where \( \epsilon_m \) represents the maximum value of power control error for all users. \( a_k(t) \) and \( b_k(t) \) are the spreading sequences and the binary data sequences for the \( k \)th user, respectively, they are given by:

\[ a_k(t) = \sum_{j=0}^{\infty} a_j^{(k)} P_{T_c} (t - T_c) \]  

(2)

\[ b_k(t) = \sum_{j=0}^{\infty} b_j^{(k)} P_{T_b} (t - T_b) \]  

(3)

Where \( T_c \) and \( T_b \) as the chip and data durations, respectively and \( P_x(y) = 1 \) for \( 0 < x < y \) and zero otherwise. \( a_j^{(k)} \) and \( b_j^{(k)} \) take the values +1 and -1 randomly and independently with equal probabilities. It is assumed that the spreading sequence is periodic with period \( N = \frac{T_b}{T_c} \) and \( a_j^{(k)} = a_{j+N}^{(k)} \) for all \(-\infty < j < +\infty\).

Channel model: In the following, it is assumed that the channel is frequency selective multipath for the uplink. The equivalent complex low-pass representation of the channel for the \( k \)th user is given by:

\[ h_k(t) = \sum_{l=0}^{L_R-1} h_{k,l} \delta(t - r_{k,l}) e^{j \eta_{k,l}} \]  

(4)

Where random variables \( h_{k,l} \), \( r_{k,l} \) and \( \eta_{k,l} \) are the \( l \)th path gain, delay and phase respectively, for the \( k \)th user. In [1], the following assumptions are considered:

For different users and pathsin each link, the random variables \( h_{k,l} \), \( r_{k,l} \) and \( \eta_{k,l} \) are all statistically independent.

The random phases \( \eta_{k,l} \) are uniformly distributed over \([0,2\pi]\) and the path delays \( r_{k,l} \) are uniformly distributed over \([0, T_b]\).

There are \( L_p \) paths for each user and these different paths are separated in time from each other by more than \( 2T_c \).

For each user, the path gain \( h_{k,l} \) is a random variable with Rayleigh distribution given by:

\[ p(h_{k,l}) = \frac{h_{k,l} e^{-\frac{h_{k,l}^2}{2\sigma^2}}}{\sigma^2} \]  

(5)

The fading rate in the channel is slow compared to the bit rate, so that the random parameters associated with the channel do not vary significantly over two consecutive bit intervals.

The received signal at the central station \( r(t) \), mixed with AWGN \( n(t) \) with two sided spectral density \( \frac{N_0}{2} \), is given by:

\[ r(t) = \sqrt{2P} \sum_{k=1}^{K} \sum_{l=0}^{L_R-1} G_k \beta_k a_k(t - r_{k,l}) b_k(t - r_{k,l}) \cos(\omega_0 t + \phi_{k,l}) + n_c(t) \cos(\omega_0 t) + n_s(t) \sin(\omega_0 t) \]  

(6)

Where \( \phi_{k,l} = \theta_{k,l} + \eta_{k,l} - \omega_0 r_{k,l} \) and the term \( n_c(t) \) et \( n_s(t) \) are low-pass equivalent components of the AWGN n(t).

Receiver model: For BPSK modulation, [4] described the structure of one of the paths of a RAKE receiver using coherent detection:

In the goal to reject MAI, a bank of single path matched filters, each of which is matched to different paths, have the same impulse response matched to \( 2\hat{a}_k(t) \cos(\omega_0 t) P_{T_b}(t) \) where \( \hat{a}_k(t) \) is the weighted despreading sequence with details given below. The outputs of all single matched filters \( \hat{x}_{k,l}(\tau) \), \( l \in [0, L_R - 1] \), where \( L_R \) is the order of diversity, are weighted the corresponding path gains and then summed to form a single decision variable \( \hat{x}_k(\tau) \). The weighted despreading function of the \( k \)th user’s RAKE receiver can be expressed as:

\[ \hat{a}_k(t) = \sum_{j=-\infty}^{\infty} a_j^{(k)} \left\{ \left[ t - jT_c / \{ j , c \} \right] \{ j , c \} \right\} \]  

(7)

Where \( c = \{ a, a \} \), \( \left[ t / \{ j , c \} \right] \) for \( 0 \leq t \leq T_c \), is the \( j \)th chip weighting waveforms for the \( k \)th receiver conditioned on the status of three consecutive chips \( \{ a, a, a \} \) and \( P_x(y) = 1 \) for
where $\gamma = (1 + \varepsilon_m)\hat{H}$, $b = (1 - \varepsilon_m)\hat{H}$ and $\hat{H}$ is the average signal to interference plus noise ratio per channel, given by \cite{4}, eq. (36):

$$\hat{H} = \left\{ \begin{array}{ll}
\frac{\gamma}{k_b} & \left[ 2\gamma(1-e^{-\gamma/2}) + \gamma(1-\gamma)e^{-\gamma/2}\right]^{1/2} \\
N & 2\gamma(e^{-\gamma/2} - 1) + \gamma(1-\gamma)^2
\end{array} \right.$$

6. Where, $\gamma$ is the parameter of the exponential chip weighting waveforms tuned to maximize $\hat{H}$, $K$ is the number of active users, $k_b$ is the signal to noise ratio, $\gamma = \bar{N}_k/N$, $N_k$ is a random variable which represents the number of occurrences of $c_j = -1$ for all $j \in [0,N-1]$ and the term $E(\Gamma\{c_j\},\gamma)$ is given by:

$$\Gamma = \left\{ \begin{array}{ll}
\frac{\gamma}{k_b} & \left[ 2\gamma(1-e^{-\gamma/2}) + \gamma(1-\gamma)e^{-\gamma/2}\right]^{1/2} \\
N & 2\gamma(e^{-\gamma/2} - 1) + \gamma(1-\gamma)^2
\end{array} \right.$$

where $\gamma$ is the number of occurrences of $\{v_j, v_{j+1}\}$ for all $j \in [0,N-1]$ in the $k$th user's spreading sequence. Each element of $\{v_j, v_{j+1}\}$ takes values $+1$ or $-1$ with equal probabilities.

A neural networks based determination: The most common neural network model is the Multi-Layered Perceptrons MLP\cite{5}. This type of neural network is known as a supervised network because it requires a desired output in order to learn. The notation R-S1-S2-S refers to a MLP with two hidden layers. The first layer have R neurons is called the input layer, the last is the output layer equipped with S neurons and the intermediate layers are the hidden layers with S1, S2 neurons. Each neuron of a layer is connected to all the neurons of the following layer (feed-forward neural network).
We associate a weighting coefficient (synaptic weight) to each connection. These weights are stored in the matrices of weight noted W1, W2 and W3 (example: R-S1-S2-S network). The element \((i,j)\) of a weight matrix represents the connection weight connecting neuron \(i\) of the downstream layer to neuron \(j\) of the upstream layer.

Each layer (except that of input) is connected to a special cell with a constant output of value 1. The corresponding weights are stored in a vector called bias and noted \(b1, b2\) and \(b3\) in the case of two hidden layers. Each neuron \(i\) of the first hidden layer computes his input \(net_1[i]\) and his output (its activation) \(a_1[i]\) as follow:

\[
net_1[i] = \sum_{p} W1[i,p] b1[i], \quad \quad a_1[i] = F1(net_1[i])
\]

Where \(W1[i]\) is the \(i\)th line of \(W1\), \(< >\) is the notation for the usual scalar product, \(p\) is the input vector and \(F1\) is the activation function associates to the first hidden layer. The activation functions are non linear and of sigmoid type, i.e:

\[
F(x) = \frac{1}{1+e^{-x}}
\]

The activations stored in the vector \(a1\) are propagated to the cells of the following layer. In a similar way, we calculate the second activation vector:

\[
a_2[i] = \sum_{a1} W2[i,a1] b2[i], \quad \quad a_2[i] = F2(a1[i])
\]

This mechanism continues to the last layer and makes it possible to obtain the output vector \(t\) corresponding to the input \(p\). The network inputs consist of vectors of size \(R\) stored in a matrix \(P\) with \(N\) columns. Each column \(p\) of \(P\) is associated a desired vector \(q\) of the output \(Q\) with size \(S\) stored in a matrix \(Q\). The outputs computed by the network are stored in a matrix \(T\).

The required goal, is the learning of associations \((p,q)\) : the network must restore the desired output \(q\) (or an output rather close to \(q\)) when the form \(p\) is presented as an input. The training of the MLP networks consists in computing the weights of connections between the neurons in order to minimise a square criterion \(E\):

\[
E = \frac{1}{N} \sum_{p=1}^{N} E_p
\]

\[
E_p = \frac{1}{2} \sum_{j=1}^{S} (Q[j][p] - T[j][p])^2
\]

For the real applications, we do not know the pace of the error function \(E\) in the space of the weights, what has as consequence when the non-linear training algorithm converges, we are never assured that the obtained minimum is global.

Backpropagation algorithm was created by generalizing the Widrow-Hoff learning rule to multiple-layer networks and non-linear differentiable transfer functions. The standard backpropagation is a gradient descent algorithm in which the network weights are moved along the negative of the gradient of the performance function \(E\). An iteration of this algorithm can be written:

\[
w(k + 1) = w(k) - \varepsilon g_w(k)
\]

Where:

\[
g_w(k) = \left( \frac{\partial E}{\partial w_1(k)}, \ldots, \frac{\partial E}{\partial w_n(k)} \right)^T
\]

The gradient error evaluated in \(w(k)\). \(n\) is the number of the connections of the network, \(k\) an index of the iteration, \(w(k) = (w_1(k), \ldots, w_n(k))^T\) is The weight vector in the iteration \(k\) and \(\varepsilon\) is a learning rate \((\varepsilon > 0)\).

Parameter \(\varepsilon\) regulates the size of the gradient step. The performance of the algorithm is very sensitive to the proper setting of the learning rate. If the learning rate is set too high, the algorithm may oscillate and becomes unstable. If the learning rate is too small, the algorithm will take too long to converge. The greatest disadvantage of this algorithm is that it does not even ensure convergence towards a local minimum\(^6\).

Several algorithms are proposed to land to this problem. In this work, we have used the Levemberg-Marquardt algorithm\(^7\) that combines the best features of Gauss-Newton and gradient descent method was used to estimate the parameters of the neural networks model (weights).

The neural networks employed has eight inputs and one output, seven of the inputs are bound directly to the used code:

\[
\hat{\Gamma}_k=[\Gamma_k^{(1)} \Gamma_k^{(2)} \Gamma_k^{(3)} \Gamma_k^{(4)} \Gamma_k^{(5)} \Gamma_k^{(6)} \Gamma_k^{(7)}], \quad \text{and} \quad \hat{\Phi}_k
\]

The last input is \(\text{snr}_k\) and the output of the neural networks model is \(\gamma\). The \(\text{snr}_k\) values of training data have been taken from the range of \([0,22]\) dB.

**NUMERICAL RESULTS**

Here, we present the numerical results of our proposed method. The used codes in Table 1 are those of Gold having \(N = 31\) for their good correlation properties\(^8,9\). The number of users is \(K = 9\), Table 2
Table 1: Code of N=31

| Code | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|------|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| Code 2 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 3 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 4 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 5 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 6 | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 7 | 1 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 8 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| Code 9 | 1 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

Table 2: Quantities $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ and $\hat{N}_k$ of the code set having N=31

| Code | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ | $\hat{N}_k$ |
|------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|------------------|
| 1    | 10                              | 10                              | 10                              | 10                              | 10                              | 10                              | 10                              | 20               |
| 2    | 2                               | 4                               | 8                               | 4                               | 6                               | 7                               | 12                               |
| 3    | 4                               | 8                               | 8                               | 4                               | 4                               | 3                               | 16                               |
| 4    | 2                               | 8                               | 8                               | 2                               | 2                               | 9                               | 12                               |
| 5    | 4                               | 8                               | 8                               | 4                               | 4                               | 3                               | 16                               |
| 6    | 2                               | 8                               | 8                               | 6                               | 6                               | 1                               | 16                               |
| 7    | 9                               | 10                              | 6                               | 3                               | 1                               | 2                               | 20                               |
| 8    | 4                               | 8                               | 8                               | 4                               | 4                               | 3                               | 16                               |
| 9    | 3                               | 10                              | 10                              | 3                               | 3                               | 2                               | 16                               |

Fig. 1: The neural network model: $\gamma$ tuned to maximize $\hat{H}$ versus their number

It gives $\Gamma^{(k)}_{\{v_1,v_2,v_3\}}$ and $\hat{N}_k$ for each code. From these datas, code 1 is used as reference to train the neural networks model employed varying $\text{snr} = k_b$. After learning, the neural networks model generalize the relation between $\gamma$ tuned to maximize $\hat{H}$ and the spreading codes varying $\text{snr}$ (Fig. 1), it was tested with unseen $\text{snr}$ values.

Figure 2 and 3 give the BER calculated by WDS generated by neural network model versus $\text{snr}$ for various values $L_R=1,2,3,4$ for coherent reception ($L_p=4, \varepsilon_m = 0$) and noncoherent reception ($L_p=4, \varepsilon_m = 0$).

It is obvious that any performance degradation does not result from using the obtained values in place of the optimal values ($\gamma$ o maximize $\hat{H}$), for these selected codes. Also, we tested the network with the other codes existing in the code set as a reference and see that it produces similar satisfactory results for those, too.

It is worth mentioning that all calculations took almost 0.1–0.4 sec on a personal computer with a Pentium IV processor running at 2.8 GHz to obtain a result against an arbitrary set of parameters. When the calculation time is considered for the optimal values, it can be said that the proposed approach is almost six
times faster than the classical technique. As a result, the neural approach is efficient and useful for the determination process of the despreading sequences weighted by exponential chip waveforms.

CONCLUSION

A new approach based on NN has been successfully presented in this study to help the determination process of the exponentially weighted despreading sequences for a DS/CDMA system. In this approach, the nearly optimal values of the parameter are simply and quickly computed. Using the results computed by the neural approach does not cause any degradation on the performance of the system. Moreover, the approach presented in this study can be used for DS-CDMA systems having different processing gain and employ exponentially weighted despreading sequences in the receivers. Even if the training time takes a few seconds, the proposed method provides simplicity after training. Instead of complicated mathematical functions, there are a number of weight multiplication and summation in the structure of the neural model. So, the neural model is very simple and useful. The obtained neural structure can be easily implemented or inserted in a neural hardware available in the market. The neural hardware might be used not only in base stations but also for mobile units.

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