Viscoelastic cluster densification in sheared colloidal gels

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Many biological materials, consumer products and industrial formulations are colloidal suspensions where the suspending medium is itself a complex fluid, and such suspensions are effectively soft matter composites. At rest, the distortion of the microstructure in the suspending fluid by the particles leads to attractive interactions between them. During flow, the presence of a microstructure in the viscoelastic suspending medium changes the hydrodynamic forces due to the Non-Newtonian and viscoelastic effects. However, little is known about the structure development, the rheology and the final properties of such materials. In the present study, a model flocculated suspension in both a Newtonian and a viscoelastic medium was studied by combined rheological and rheo-confocal methods. To this extent micrometer-sized fluorescent PMMA particles were dispersed in polymeric matrices (PDMS). The effect of fluid viscoelasticity is studied by comparing the results for a linear and a branched polymer. Stress jump experiments on the suspensions were used to de-convolute the rate dependence of the viscous and elastic stress contributions in both systems. These results were compared to a qualitative and quantitative analysis of the microstructure during flow as studied by fast structured illumination confocal microscopy, using a counter-rotating rheometer. At comparable interaction strength, as quantified by equal Bingham numbers, the presence of medium viscoelasticity leads to enhanced densification of the aggregates during steady-state flow, which is reflected in lower limiting high shear viscosities. Following a strong preshear the structural and mechanical recovery is also altered between the Newtonian and viscoelastic matrix with a increase of the percolation threshold, but with the potential to build stronger materials exploiting the combination of processing history and medium rheology at higher volume fractions.

Introduction

Many technological and commercial materials consist of solid particles suspended in liquid suspending media. The latter is often complex by itself, and applications for particulate suspensions in a viscoelastic medium are widespread ranging from engineering materials to commercial resins, nanocomposites, commercial detergents, food formulations or cosmetics. Inks consisting of particles dispersed in a viscoelastic matrix can be found in the fabrication of ceramic thick films with inkjet printing technology or in 3D food printing. During the lifetime or processing of such products, the microstructure development and also the rheological properties play an important role.

The presence of a complex microstructure entails two aspects which complicate the rheology and processing of such materials. First, it is very difficult to obtain colloidally stable dispersions in a microstructured matrix. For example in polymeric matrices, autophobic dewetting makes even steric stabilization no longer universally robust. The polymer mediated behaviour is rich and can lead to depletion and bridging in concentrated polymer solutions and melts. Aggregated structures are hence more the rule than the exception. Second, the presence of medium viscoelasticity modifies the hydrodynamic interactions which will influence flow induced structures. The combined presence of aggregated structures and medium viscoelasticity is expected to lead to a complex microstructural response to flow fields.

Medium viscoelasticity will change the forces acting upon and in between particles and aggregates. A striking example of the modification of hydrodynamic interactions can be found in the long standing observations of flow aligned particle strings formed in suspensions of non-Brownian particles in viscoelastic media, even for conditions where Newtonian matrices would be in the dilute limit. Such strings have been observed for a wide range of suspending fluids, flow geometries and particle concentra-
 Insights on how viscoelastic and non-Newtonian effects influence hydrodynamic forces were obtained from combined experiments and simulation studies on single particles and doublets. The viscoelastic nature causes the stress to build up more gradually, causing the torque to "grab on" to the particle later compared to the Newtonian case, and more importantly the pressure field will be affected by the presence of normal stress differences reflecting the elastic nature of the fluids, with stress enhancements typically near the poles of the particles. Shear thinning enhances these normal stress effects by its effect on the local velocity gradients. The intricate coupling between pressure and velocity makes this a highly non-linear problem. A key role is played by the requirement for the particles and aggregates to obey the zero torque condition. When particles do not touch, they rotate individually in the string, albeit at a lower pace. When particles touch, the orbits of the doublets and aggregates resemble those of Jeffery orbits. At very high elasticities complex orientational cascades are observed, in agreement with an analysis based on the second order fluid by Leal and coworkers. For doublets or triplets or even more aggregated structures in viscoelastic media, vorticity oriented structures were detected by optical microscopy and small-angle light-scattering (SALS). Clearly the viscoelastic media are such that under shear flow do not improve the spatial dispersion of aggregated structures.

The complex geometry of the aggregates in flocculated suspensions further complicates matters. Several studies have investigated how flow in aggregated systems dispersed in Newtonian matrices can change the shape, size and spatial distributions of floc. For individual aggregates, hydrodynamic forces change the aggregate size and the aggregate density, mainly by erosion and fragmentation. The internal structure of the aggregates changes as a function of shear rate which also changes the streamlines in and out of the aggregates, which in turn affects erosion and breakup. At higher concentrations, flow induces large scale heterogeneity and an anisotropic microstructure with predominant orientation in the vorticity direction. Such effects have been observed, albeit qualitatively in particle suspensions in viscoelastic polymer melts. Overall, from literature it can be concluded that the interplay of flocs with shear flow leads to aggregates with decreasing size and increased density as the shear rate is increased, with an anisotropic microstructure at higher volume fractions.

The microstructural features are also expected to be reflected in the rheological properties of such systems. Again systematic knowledge is available, for either aggregated suspensions or suspensions in viscoelastic media, not of combinations thereof. For aggregated suspensions fractal models have been successful in predicting the gel storage modulus based on floc fractal dimension $D_f$, for low to moderate concentrations. At higher volume fraction, locally dense, iso-static clusters have been suggested to be acting as the load bearing units. The number of particle-particle contacts between clusters and the interaction between two particles at contact are found to be the source leading to the gel's elasticity. The flow history also plays an important role. Koumakis et al. showed that fully breaking the structure, leads to more homogeneous and stronger gels, whereas preshear at low rates creates largely heterogeneous weaker gels with reduced elasticity. In the present work we demonstrate how medium viscoelasticity provides a tool to further control the gel strength by densifying the basic aggregates even more.

The interplay between flow, floc structure and medium viscoelasticity is as yet unknown and is the subject of the current work by using adequate model systems and advanced rheological and microstructural measurements. Rheological measurements have been used to map out the flow behaviour, with the use of stress jump measurements in both suspensions in a Newtonian and viscoelastic matrix, in order to distinguish between the contribution of flocs and medium viscoelasticity. A fast high-resolution rheo-confocal setup was employed to monitor both the microstructure and the rheological behaviour simultaneously during steady state and transient flows. The size, local structure and effective volume fraction of the aggregates is measured from the confocal images and correlated to the steady state rheology. Finally, we investigate the effects of flow history and particle volume fraction on gel strength.

**Materials and Methods**

**Materials**

Spherical monodisperse polymethyl methacrylate particles with a diameter of 1.4 $\mu$m (PMMA14) were obtained from MCAT GmbH or synthesized following the protocols and used as model colloidal particles. They were sterically stabilized by chemically grafted polyhydroxy stearyic acid chains (PHSA) and provided as stock suspensions in isohexane. Two different polymeric polydimethylsiloxane (PDMS) matrices of different architecture were used: a low molecular weight PDMS with linear chains (Rhdor-sil Oils 47) and a PDMS consisting of shorter but branched chains (PDMSB86, experimental grade of Dow Corning). Their zero shear viscosity was around 5 Pa·s at 25 °C. Within the shear rate window considered, the linear PDMS displayed Newtonian behaviour whereas the branched matrix behaved as a viscoelastic shear-thinning fluid.

The PMMA-PHSA particles were dispersed in decalin (cis-decahydro naphthalene, Tokyo Chemical Industry) by several centrifugation steps at 1700 g to improve refractive index and density matching. Subsequently the suspension of PMMA-PHSA in
decalin was added in four steps to both polymer matrices. These four steps were necessary to ensure a good degree of dispersion of the particles in the more viscous matrices. Every step consisted of first a global homogenization, obtained by 5 min of vortex and hand mixing with a spatula, and subsequently high-intensity dispersing for 15 min with a high-shear mixer run at 3800 rpm (Ultra-Turrax T25 S25N-10G, IKA-Werke GmbH). Particle suspensions were never fully dried to avoid the formation of irreversible aggregates and hence some decalin was left. Therefore, suspensions of PMMA-PHSA particles, at 10, 20, 30 and 40 vol%, in a matrix consisting of 84 wt% of PDMS (linear or branched) and 16 wt% of decalin were prepared. Evaporation of decalin was not observed over the course of the experiments.

Aggregates were observed in both linear and branched matrix fluids, indicative of attractive interactions. Given the magnitude of the yield stress and particle size, the experiments during flow explore a parameter range which can be best expressed by non-dimensional numbers. The Péclet (Pe) number based on the single particle diameter, compares the rate of advection due to shear with the Brownian relaxation of particles present as individuals, and is of relevance when the structure has been completely broken down. The Bingham number, a dimensionless group defined here as $B_i = \frac{\sigma_0}{\sigma}$, compares the hydrodynamic stresses to the structural stresses, which are due to the attractive interactions when aggregates are present. The interaction strength can be related to the magnitude of the yield stress, which is proportional to the maximal attractive interparticle force, i.e., the maximum coordination number was used to describe the local structure. Experimentally, we could study the structural evolution during steady state and transient flows in the flow-vorticity plane over a wide array of length scales. In all confocal images, flow and vorticity direction are defined as $v$ and $\nabla \times v$ respectively.

### Rheology

Steady-state, transient flow and oscillatory rheological measurements were carried out with a rotational strain-controlled ARES-G2 rheometer (TA instruments), allowing to capture fast transients of the experimental system, and a stress-controlled MCR 502 WESP rheometer (Anton Paar) mounted on a confocal microscope (next paragraph). A cone-plate fixture (ARES-G2: diameter 50 mm; MCR 502: diameter 15 mm) was used for all the experiments in order to ensure a homogeneous flow field within the sample. The temperature was always kept at 20.0°C. With the standard cone-plate geometry on the ARES-G2, the shear stresses $\sigma_2$ as well as the first normal stress difference $N_1 = \sigma_{11} - \sigma_{22}$ can be measured. The second normal stress difference $N_2 = \sigma_{22} - \sigma_{33}$ was determined using a cone-partitioned plate (CPP) fixture using an MCR 702 rheometer (Anton Paar).

A preshear step of 100 s$^{-1}$ ($\dot{\gamma}_{Pe} = 375 000$, $B_{iN} = 117$; $\dot{\gamma}_{Pe} = 320 000$, $B_{iV} = 110$) was applied in order to erase the shear history and to set a reproducible initial condition for the different suspensions for a volume fraction ($\phi$) of 0.10 for which most experiments were carried out. After the preshear, the sample was allowed to rest for 3600 s before commencing measurements. At higher volume fractions shear fracture limited the highest shear rates, for $\phi = 0.2$ to 0.3 a maximum shear rate of 10 s$^{-1}$ ($\dot{\gamma}_{Pe} = 38 000$, $B_{iN} = 12$; $\dot{\gamma}_{Pe} = 45 000$, $B_{iV} = 11$) was used. For the highest volume fraction the sample was just sheared to steady state.

### Confocal microscopy combined with rheology

A fast high resolution rheo-confocal setup was used to study the microstructure and rheological behaviour simultaneously. The setup consists of a TwinDrive MCR 502 WESP rheometer (Anton Paar). The rheometer electronics are separated from the rheometer so that the supporting plate can be exposed for the confocal setup and counter-rotation is executed by means of a second motor placed in a separate holder. During a steady shear experiment, the counter-rotation of upper and lower geometry can be tuned by changing their relative velocity with a dial. Therefore, by changing the ratio of the two velocities, the stagnation plane can be moved freely in real time along the shearing gap. A standard cone-plate upper arrangement with a diameter of 15 mm and a cone angle $\beta$ of 6° was used. The lower plate consists of a transparent glass coverslip of 22 mm that is clamped down in the shear cell. The confocal setup comprises an instant structured illumination (iSIM) confocal scanner by Visitech International coupled to a Nikon Eclipse Ti-E inverted microscope. The iSIM confocal scanner allows acquisition rates up to 1000 full frames per second. A dual camera arrangement allows to image at either very small pixel sizes, with an ORCA flash 4.0 V2 from Hamamatsu, or at the highest acquisition rates by using a Lambert Instruments HiCAM 540 M/S. Imaging was performed by using a high magnification, high numerical aperture Plan Apo $\lambda$ Nikon oil objective (60x, 1.4 NA), which has a depth of field of 0.4 $\mu$m and allows a field of view of 154 x 154 $\mu$m. The objective was focused in the sample at 10 $\mu$m from the glass coverslip and at 1 mm from the center of the upper geometry. By means of the high speed confocal microscope, using counter-rotating plates and structured illumination optics, we could study the structural evolution during steady state and transient flows in the flow-vorticity plane over a wide array of length scales. In all confocal images, flow and vorticity direction are defined as $v$ and $\nabla \times v$ respectively.

### Image quantitative

Quantitative 2D image analysis was performed by adapting standard algorithms for particle tracking for extracting particle coordinates. Briefly, the algorithms consist of background subtraction and Gaussian filtering, which results in locating particle centroids in the 2D image based on local intensity maxima. Finally, the centers are refined to subpixel accuracy based on moments of the local intensity distribution.

At high shear rates, flow breaks down the particle network to single particles or small clusters of particles. In this regime, the coordination number was used to describe the local structure. The coordination number can vary between zero and six in two dimensions. In addition coordination number distributions are used to quantify cluster size distributions. Particles are consid-
erred to be in contact if their center-to-center separation is smaller than the first minimum of the radial pair distribution function of a fully developed gel. Given the field of depth of about 140 nm with the highest NA objective, this is somewhat arbitrary, but as we are mainly interested in comparing the relative differences.

When reducing the shear rate, the microstructure changes and, depending on particle volume fraction and interparticle interactions, larger isolated clusters or even a 3D network form. In this case it is more relevant to quantify the heterogeneity of the microstructure. The number density fluctuations as a function of box size were used as a descriptor. The latter is defined as the integrated pair correlation function and is determined by placing boxes of different sizes on the image and counting the particles inside. Therefore, the number density variations are defined as the variance in the number of particles, \( N(A) \), calculated for a fixed box size of area \( A \) in different frames and normalized by the mean number of particles in that box:

\[
\frac{\langle N(A)^2 \rangle - \langle N(A) \rangle^2}{\langle N(A) \rangle}.
\]

The boxes were placed randomly at 100 different positions for each frame. Boxes with a side length (d) ranging from one particle diameter (2a) to a maximum of 1/5 of the total image size were used. The number of frames chosen for a good averaging was such that considering additional frames would not change the result. Changes in the number density fluctuations correspond to gradients in the local density or heterogeneities in the structure, and the associated length scales can be identified as a characteristic length scale of the heterogeneous structure. Box sizes where the number density fluctuations become approximately constant indicate length scales on which the density is homogeneous. This measure is directly related to the compressibility of the suspension and equal to the low-\( q \) limit of the structure factor. To quantify the anisotropy of the images at relatively high shear rates, their FFT was calculated using Image-J.

**Results and discussion**

**Matrix rheology**

Experimental data for the steady-state viscosity \( \eta \) and stress ratios corresponding to the first and second normal stress differences, \( N_1/\sigma_{33} \) and \(-N_2/\sigma_{22} \), as a function of shear rate \( \gamma \) are shown in Fig. 1 for the Newtonian and viscoelastic matrices. The matrix consisting of linear PDMS and cis-decalin behaves as a Newtonian fluid (N), with a constant viscosity as function of shear rate. Instead, the matrix consisting of branched PDMS and cis-decalin behaves as a viscoelastic shear thinning fluid (VE) (Fig. 1), showing a decreasing viscosity as a function of shear rate. As expected, the Newtonian matrix did not show any normal stress difference, hence no stress ratio could be evaluated. Unlike the Newtonian matrix, at shear rates above 10 s\(^{-1}\) the viscoelastic matrix shows measurable first and second normal stress differences.

\( \eta \) results in a positive stress ratio whose value increases above 1 at 100 s\(^{-1}\), meaning that at high shear rates we enter in a relatively high Wi regime. As expected, the viscoelastic polymer matrix shows a positive \( N_1 \) and a negative \( N_2 \) whom absolute modulus is increasing with the shear rate. The first normal stress difference, \( N_1 \), measures the difference in normal stress between the flow and gradient directions, while the second normal stress difference, \( N_2 \), measures the difference in normal stress between the gradient and vorticity direction. Physically, a positive \( N_1 \) and negative \( N_2 \) means that the elastic stresses are anisotropic, typical of a polymer matrix, and the stress tensor of the matrix is flow-oriented.

**Steady-state microstructure and stress contributions**

The flow curve (shear stress versus shear rate) of the suspension is shown in Fig. 2(a) along with the flow curve of the matrix, which is plotted as a comparison only at high shear rates. It shows the typical behavior of an aggregated suspension with a yield stress and an increase of viscosity at higher shear rates, compared to the matrix viscosity. Dullaert and Mewis have used stress jumps to clarify how the non-Newtonian behaviour of the suspension finds its origin in the stress dependent microstructure, which changes from a percolating network with essentially solid like response to a fluid system containing small dispersed aggregates at low volume fraction. The origin of these viscous and elastic stress contributions to the overall stress in such suspensions is described in the works of Doi et al. and Potanin and coworkers. To measure such stress jumps, a rheometer with a force rebalanced transducer (ARES G2) was used. The experimental protocol consists of a pre-shear step until steady state is reached at a certain initial value of shear rate, \( \gamma_0 \), followed by a step down in shear rate to a final value of 0.0001 s\(^{-1}\), as explained in (an example can be found in Fig. S1 in Supporting Information). The final shear rate chosen was not 0 s\(^{-1}\) but an almost-zero value due to some specific instrumental issues with drift at zero shear rate. The experimental response in the first 30 ms cannot be taken into account since it is related to the response of the mechanical and electronic components of the rheometer, even when signal filtering is reduced. The viscous and elastic contributions were calculated by performing a log-linear regression of the data between 30 ms and 70-100 ms and determining the intercept (an example can be found in Fig. S2 in Supporting Information). After 100 ms the thixotropic recovery of the material starts interfering with the viscoelastic response of the material, setting the limit of data range that can be used for the calculation of stress contributions.

Stress jump experiments for a suspension of 10 vol% PMMA in the Newtonian matrix resulted in rate dependent viscous and elastic stresses as reported in Fig. 3, along with the total stress response at steady state. These results are in line with data on suspensions of fumed silica in paraffinic oil and poly(isobutylene) by Dullaert and Mewis, with the responses at low deformation rates being elastic in nature. Indeed from the stress jump measurements it results that at very low shear rates, 0.01 (\( P_{\text{EN}} = 35, B_{\text{IN}} = 0.01 \)) up to 0.063 s\(^{-1}\) (\( P_{\text{EN}} = 200, B_{\text{IN}} = 0.07 \)), the steady state shear stress, hence the apparent yield stress of 5 Pa,
is elastically-dominated. The microstructure was visualised by using the rheo-confocal setup, so that a qualitative relation with the stress contributions can be found. The corresponding microstructures at 0.025 (\(Pe_N = 95, Bi_N = 0.03\)) and 0.063 s\(^{-1}\) (\(Pe_N = 200, Bi_N = 0.07\)) are shown in Fig. 2b and 2c respectively. At these shear rates the stress is elastic and it emerges from big particle clusters that interconnect. As the rate is increased the elastic stress component decreases, but the viscous (hydrodynamic) part of the stress starts to become dominant. Fig. 2d shows the structure at 0.25 s\(^{-1}\) (\(Pe_N = 950, Bi_N = 0.3\)) as the bonds between flocs are lost, and there are mostly large isolated clusters. Fig. 2e shows that at this point the viscous stress becomes higher than the elastic one. When going to intermediate shear rates like 1 s\(^{-1}\) (\(Pe_N = 4000, Bi_N = 1.2\)), the system enters a purely viscous region where elastic stresses tend to zero and hydrodynamic stresses dominate. Therefore the elastic stresses could not be detected anymore above 1 s\(^{-1}\). Fig. 2f shows that isolated clusters are the main microstructural units. In line with literature\(^{20,23-24}\) these flocs are getting smaller in size, compared to Fig. 2d, because subject to higher Pe numbers. At relatively high shear rates, for instance at 20 s\(^{-1}\) (\(Pe_N = 75000, Bi_N = 24\)), flocs are broken down almost fully. Fig. 2g shows that, at these shear rates, the microstructure is made of small clusters of particles tumbling as a whole and aligning in vorticity direction. In this region the stress is purely viscous as shown in Fig. 2h.

The same rheological and microstructural analysis was performed for 10 vol% PMMA dispersed in the viscoelastic matrix (Fig. 3). Also in this case at low shear rates, for instance at 0.025 s\(^{-1}\) (\(Pe_{VE} = 135, Bi_{VE} = 0.03\)), the stress is purely elastic and the viscous contribution is negligible. Fig. 3a shows the microstructure at such low shear rate, which from a first analysis appears to be very similar to the Newtonian case, with flocs of particles interconnected and probably forming a 3D spanning network. Increasing the shear rate up to 0.16 s\(^{-1}\) (\(Pe_{VE} = 850, Bi_{VE} = 0.17\)), the number of inter-floc bonds seem to decrease leading to a more heterogeneous microstructure consisting of big flocs and large voids, as shown in Fig. 3b. Here, at 0.16 s\(^{-1}\), the viscous contribution becomes comparable to the structural (elastic) one. When increasing the applied shear rate up to 0.4 s\(^{-1}\) (\(Pe_{VE} = 2000, Bi_{VE} = 0.44\)), the plot in Fig. 3c shows how the suspension enters the region where the viscous contribution becomes dominant. The corresponding microstructure is shown in Fig. 3d, with flocs appearing more isolated and smaller in size. For the Newtonian matrix, a shear rate of 1 s\(^{-1}\) (\(Pe_N = 4000, Bi_N = 1.2\)) was enough to create a purely hydrodynamic stress. When particles are suspended in a viscoelastic matrix this is not unexpectedly different. Indeed, at 1 s\(^{-1}\) (\(Pe_{VE} = 5000, Bi_{VE} = 1.1\)) in a viscoelastic matrix, the elastic contribution to the stress starts increasing again along with the shear rate. However, the elastic stress in this case is coming from the matrix and not from the particulate structure. Qualitatively the aggregates are not differing much from the case of the suspension in the Newtonian matrix (Fig. 2f), with isolated relatively small flocs, however the stress is partially elastic whereas, in the Newtonian matrix,
it was purely viscous. At 20 s\(^{-1}\) \((\text{Pe}_V = 80000, \text{Bi}_V = 22)\), the formation of small clusters of particles oriented in vorticity direction is also detected (Fig. 3), but unlike the Newtonian case, here a measurable elastic stress is generated exclusively from stretching the polymer chains of the matrix (Fig. 3b). Overall, at such high shear rates the viscous stress is however still almost an order of magnitude higher, indicating that the hydrodynamic stress still dominates. The elastic and viscous contribution in the branched matrix fluid are shown in Fig. S3 in Supporting Information.

### Cluster densification and rheological properties

When focusing the analysis on the suspension microstructure at high shear rates, for instance at 20 s\(^{-1}\) (value at which the Pe numbers in the two suspensions are comparable), the formation of dense aggregates tumbling as a whole and some moderate alignment in vorticity direction is observed in both cases, as expected for aggregated systems\(^{18,22}\) (Fig. 4). In Fig. 4, typical particle arrangements in the two different matrices at 20 s\(^{-1}\) \((\text{Pe}_N = 75000, \text{Bi}_N = 24; \text{Pe}_V = 80000, \text{Bi}_V = 22)\) as well as the corresponding FFT’s are shown. The denser clusters forming in the viscoelastic matrix seem to stronger orient in the vorticity direction (Figure 4 (b)). Indeed, by computing Fourier transform of the images, at small wave vectors a more pronounced vorticity alignment is also detected (Fig. 3f), but unlike the Newtonian case, the formation of small clusters of particles oriented in vorticity direction is also observed in both cases, as expected for aggregated systems\(^{18,22}\).

This cluster densification can be rationalised based on the indirect effects of the normal stress differences and the resulting changes in the disturbance velocity fields around the particles\(^{18,19,31}\). Every data point of the plot is averaged over around 4000 particles and the probability is normalised by the total number of particles so that a comparison of the two cases can be made. In the viscoelastic matrix, although the clusters seem to densify, the 2D average coordination number stays low (around 2.3). However, such a small average coordination number derives from the relatively small average size of the clusters, with the bigger clusters consisting of approximately 10 particles.

Clusters and cluster size distributions can be derived by using the particle positions and distances obtained through confocal imaging. Based on cluster size distributions, an effective volume fraction can be calculated, which is 0.27\(\pm\)0.02 for suspension in the Newtonian matrix and 0.23\(\pm\)0.02 in the viscoelastic one. The stress jump experiments of Fig. 2 and Fig. 3 showed that in both classes the hydrodynamic stress dominates at high Pe, therefore the effective volume fraction can be obtained from the relative high shear viscosity as well. The effective volume fraction, \(\phi_{\text{eff}}\), can be calculated from\(^{67}\)

\[
\eta_{\infty} = \left(1 - \frac{\phi_{\text{eff}}}{\phi_{\text{max}}}\right)\frac{|\eta|\rho}{\phi_{\text{max}}},
\]

with \(\eta_{\infty}\) is the relative high shear viscosity, the factor \(|\eta|\rho\) is equal to 2.5 for spheres case\(^{69}\) and the maximum packing fraction \(\phi_{\text{max}}\) is equal to 0.64 (since the effective filler packing limit is unknown, the case of fully dispersed hard spheres has been used). In this way an effective hydrodynamic volume fraction of 0.28 is obtained for the suspension in the Newtonian matrix and 0.24 for the one in viscoelastic matrix, for equal
mass fraction. These values compare well with the cluster volume fractions measured by confocal microscopy. A sheared viscoelastic matrix leads to denser clusters and a lowering of the high shear viscosity, at equal mass concentration of particles.

This denser local aggregate structure is also reflected in subsequent network structures formed following preshear. If the shear rate is stepped down to a value of 0.025 s\(^{-1}\) (\(Pe_N = 95, Bi_N = 0.03\); \(Pe_VE = 135, Bi_VE = 0.03\)), the number density fluctuations can be studied to assess sample heterogeneity. Fig. 5 shows that, at larger length scales, number density fluctuations are enhanced for particles suspended in a viscoelastic matrix, which indicates an increased compressibility and the existence of larger voids. While in classical depletion systems heterogeneities are shown up to length scales of 10 to 20 particle diameters at most, when suspending particles in a polymer matrix, structures at length scale of 100 particle diameters are developing. Moreover, the analysis of the number density fluctuations suggests different cluster architectures forming in the two matrices at low shear rates. Particularly more open aggregates seem to develop in the Newtonian matrix. Therefore, even at low \(Pe\) numbers and negligible stress ratio more compact clusters and larger voids are forming in the viscoelastic matrix. These more compact flocs come from the preshear step performed at high shear rates. The cluster densification induced during preshear is consistent with the shear-induced microstructural evolution observed previously in other colloidal dispersions, such as carbon black suspensions\(^{53,71}\) amongst others.

Making stronger gels

The results in the previous sections, as in Fig. 5 and 6, showed that denser aggregates are formed in strongly sheared viscoelastic matrices. The density of the aggregates lowers the effective volume fraction as was inferred both from the high shear viscosity and the confocal images (Fig. 5). It can be expected that these denser network building blocks increase the percolation threshold when compared at overall volume fraction. On the other hand, recent work on colloidal gels\(^{68}\) has demonstrated that gel elasticity is controlled by the volume fraction of locally isostatic clusters, which can be expected to increase more strongly with volume fraction in the denser systems. Here, the change in percolation threshold and volume fraction dependency of gel elasticity are shown to be linked.

To set a reproducible initial condition, a preshear step at 100 s\(^{-1}\) (\(Pe_N = 375 000, Bi_N = 117\); \(Pe_VE = 320 000, Bi_VE = 110\)) was performed for the model suspensions of 10 vol\% PMMA in both matrices, leading to the formation of denser building blocks in the viscoelastic matrix at high shear rates (Fig. 5). The build-up of the gel microstructure was monitored for approximately 3 hours by applying amplitude oscillatory flow in the linear viscoelastic region and it is shown in Fig. 7(a). For the suspension in the Newtonian matrix, the loss modulus is initially higher than the storage one, and the values stay constant for a few minutes. Subsequently, the moduli start to evolve over time, with \(G''\) initially lower than \(G'\), until they cross each other. Eventually the storage modulus becomes higher than the loss modulus. A different picture emerges when using as suspending media a viscoelastic matrix. Both moduli appear to level off already at the beginning of the recovery step and the loss modulus remains dominant even after 3 hours. An explanation for this lies in a change of the percolation limit. Indeed, the formation of denser
clusters in the viscoelastic matrix results in a different number of single particles. In order to test whether the percolation limit really plays such a dominant role, the moduli evolution during the gel build up step was monitored at higher particle loadings as well.

Fig. 2(b) reports the gel recovery step but for suspensions with a particle volume fraction of 40 vol%. Notice that, at this concentration, the preshear step was performed at a shear rate of 0.1 s\(^{-1}\) \((P_eN = 380, B_iN = 0.12; P_eVE = 535, B_iVE = 0.11)\) only, due to the occurrence of shear fracture at higher shear rates. Already at the very beginning of this recovery test, the storage modulus results higher compared to the loss modulus, in both suspensions. At high particle content the storage modulus increases over time in both the Newtonian matrix and the viscoelastic one, following a power law relation. Another important outcome concerns the fact that, at higher concentrations, the storage modulus is greater when PMMA particles are dispersed in a viscoelastic matrix rather than a Newtonian fluid. This result suggests that when increasing the volume fraction, stronger gels can be formed by exploiting the viscoelastic shear densification. Unfortunately these higher volume fractions could not be imaged sufficiently clear to provide a quantitative comparison.

The dynamic test has been performed at intermediate particle volume fractions as well. Fig. 3 displays the value of storage modulus, \(G'\), reached after 3 hours of recovery as a function of volume fraction. Notice that the dash dot lines are just there to guide the eyes. The steady state value of the storage modulus seems to increase monotonically with the volume fraction, and with different slopes in the two matrices. Koumakis and Petekidis distin-
guished different behaviour at low and high φ. Here, at relatively low volume fractions for a cluster fluid (φ = 0.1), using a Newtonian rather than a viscoelastic matrix creates the strongest gels, as the distance to the percolation threshold is larger. However, increasing the filling volume fraction, in the existence region of the transient percolated network (0.1 < φ < 0.3), the moduli become more and more similar until a crossover point as the higher density to the clusters leads to a stronger dependency on volume fraction. Eventually, at high volume fractions when the material exhibits a solid-like response (φ = 0.4), as already seen before, viscoelasticity compacts the flocs and boosts the storage modulus.

The rheological properties of the fully developed gels also reflect this difference in aggregate structure. Rheological properties can be used to characterize the gel structure, by using a fractal scaling theory. For fractal gels, Shih et al. defined two regimes, depending on whether links between different fractal flocs, the inter-floc links, are stronger or weaker than bonds within a floc, the intra-floc bonds. In both regimes, albeit with different expressions for the exponents, G' increases with the volume fraction following a power law, which for fractal gels depends on the fractal dimension Df:

\[ G' \propto \phi^{D_f}. \]  

In the fractal regime, the fractal dimension should reflect the density of the aggregates in the different matrices and it was fitted based on the lowest volume fraction experimental data (Fig. S4 in Supporting Information) using the model of Wu and Morbidelli. The gels made with presheared viscoelastic materials are more "brittle" and the moduli shows a stronger dependency on volume fraction, consistent with the confocal observations of denser aggregates. Although not all gels belong to the fractal regime (too high volume fractions) it is helpful to look at the "effective" fractal dimension obtained from the analysis which is found to be Df = 2.3 for the suspension in Newtonian medium and Df = 2.6 for the suspension in the viscoelastic suspending medium. The lower fractal dimension for the suspension in the Newtonian matrix suggests that the more open aggregates compared to the ones in the viscoelastic matrix are retained in the final gel properties. Finally, the lower fractal dimension, and thus the formation of more open flocs, rationalize the trend towards a lower percolation threshold in the Newtonian matrix, and therefore the different trend of moduli during recovery in the two matrices.

Conclusions

The viscoelasticity of the suspending matrix changes the local torque and pressure distribution around single particles or particle aggregates. For both a Newtonian and a viscoelastic matrix, the subsequent shear rate dependent microstructures in the flow-vorticity plane and the resulting rheological properties have been studied, by using of a homemade rheo-confocal setup. By performing stress jump experiments the elastic and viscous contributions to the total stress at steady state have been separated, revealing a complex interplay between particles and the viscoelastic
matrix. At equal viscous strength (comparable Pe numbers) but different stress ratios, the microstructural analysis showed that denser clusters are developed in a viscoelastic matrix. Furthermore, from the evolution of the viscous stresses at high shear rates, cluster densification in a viscoelastic matrix could be inferred from a lowered effective volume fraction. When comparing gels at equal volume fraction, the cluster densification has two opposite effects for the structural recovery, on one hand the percolation threshold in the densified systems is increased, but on the other hand, the aggregate contributions once in a network are stronger. In viscoelastic media, processing gels at low volume fractions leads to weaker gels compared to particles at the same attraction strength in Newtonian media, but stronger gels are obtained for higher volume fractions. This adds medium viscoelasticity as a parameter to be considered when designing colloidal gels.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

PVP and RM acknowledge funding of KU Leuven GOA/05/007 project. This project has received funding from the European Unions Horizon 2020 research and innovation programme under grant agreement No 731019 (EUSMI).

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The effect of medium viscoelasticity on microstructure and rheology of flocculated suspensions was studied by rheological and rheo-confocal methods. Cluster densification under flow mainly affects high shear viscosities and material strength.