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Due to the high energies and long distances to the sources, astrophysical observations provide a unique opportunity to test possible signatures of Lorentz invariance violation (LIV). Superluminal LIV enables the decay of photons at high energy. The High Altitude Water Cherenkov (HAWC) Observatory is among the most sensitive gamma-ray instruments currently operating above 10 TeV. HAWC finds evidence of 100 TeV photon emission from at least four astrophysical sources. These observations exclude, for the strongest of the limits set, the LIV energy scale to 2.2 \times 10^{13} \text{ eV}, over 1800 times the Planck energy and an improvement of 1 to 2 orders of magnitude over previous limits.
Introduction. – The precise measurements of very high energy (VHE) photons can be used as a test for fundamental physics, such as the Lorentz symmetry. As for any other fundamental principle, exploring its limits of validity has been an important motivation for theoretical and experimental research. Lorentz invariance (LI) powerfully constrains fundamental interactions of particles and fields. Moreover, theories that go beyond the standard model of particles (SM), such as quantum gravity or string theories, can motivate Lorentz invariance violation (LIV) [1–11]. Therefore, the dedicated experimental tests of such effects may also help to clear the path to a unification theory of the fundamental forces of nature. Small LIV effects might occur with unrelated magnitudes in different sectors such as gravitational wave propagation, interactions of gravity and matter, or light propagation. In the photon sector, some effects of LIV are expected to increase with energy and over long distances due to cumulative processes in photon propagation. Therefore, astrophysical searches provide sensitive probes of LIV and its potential signatures, such as energy-dependent time delay, photon splitting, vacuum Cherenkov radiation, photon decay, and many other phenomena [12–20].

The High Altitude Water Cherenkov (HAWC) Observatory is a wide-field-of-view array of 300 water tanks, each containing four photomultiplier tube detectors. HAWC is located at 4100 m above sea level at 19° N near the Sierra Negra volcano, in Puebla, Mexico, covering an area of 22,000 m². Since 2015, HAWC has operated with a live fraction duty cycle greater than 95%. HAWC recently reported detailed measurements of gamma-ray emission above 100 TeV [21, 22], made possible thanks to the development of advanced energy reconstruction algorithms, including one using an artificial neural network (NN).

The HAWC observations of high-energy photons in several locations across the sky creates the unique opportunity to test LIV, through the precise measurement and reconstruction of these VHE photons. Previous studies of possible LIV constraints with HAWC have indicated its special utility in LIV searches. For instance, Ref. [23] analyzes the possibility to test energy-dependent time delays through GRB and pulsar measurements, which would result in strong limits on LIV in the photon sector. In [24], the potential of LIV photons to decay to $e^+e^-$ was explored. Further preliminary results were presented in [25, 26].

Superluminal LIV allows photon to decay at high energies. Photon decay to light fermions proceeds over short distances (centimeters or less) once above the energy threshold of the process [12–17]; which would lead to a hard cutoff at high photon energies in astrophysical spectra [27]. Another process, the photon decay into multiple photons [19, 20, 28], also predicts a significant reduction of the photon flux at VHEs beyond which no photons should reach the Earth from astrophysical distances.

In this work, we study four Galactic sources to determine whether there is a hard cutoff compatible with LIV photon decay in the observed spectra of each source. We find that none of them favor such a phenomenon, and we use recent observations of photons above the energy of 100 TeV with HAWC to improve LIV limits by 1 to 2 orders of magnitude over previous values [12, 19, 29]. In the next section, we present the highlights of LIV photon decay phenomena. Then, we describe the analysis and present our results, assess systematic uncertainties and sensitivity of our measurements, and finally, present our conclusions.

Lorentz Invariance Violation – The introduction of a Lorentz violating term in the SM Lagrangian or spontaneous Lorentz symmetry breaking can induce modifications to the particle dispersion relation, compared to the standard energy-momentum relationship in special relativity [11, 14, 30]. Although there are various forms of modified dispersion relation (MDR) for different particles and underlying LIV-theories, several of them lead to similar phenomenology, which can be useful for LIV tests in extreme environments such as the astroparticle scenarios we consider here [12, 14, 28, 30–32]. Phenomenologically, the LIV effects can be generalized as a function of energy and momentum. In this way, a family of effective MDRs can be addressed for different particles. The MDR for photons is

$$E^2 - p^2 = \pm |\alpha_n| p^{n+2},$$  \hspace{1cm} (1)

where $(E_\gamma, p_\gamma)$ is the photon four-momentum, $\alpha_n$ is the LIV parameter, $n$ is the leading order of the correction from the underlying theory, and $p_\gamma \approx E_\gamma$ at first order in $\alpha_n$ [33–38]. The sign usually refers to the so-called superluminal ($+$), and subluminal ($-$) dominant phenomena. For $n > 0$, limits on the LIV parameter $\alpha_n$ can be interpreted in terms of some LIV energy scale,

$$E_{LIV}^{(n)} = \alpha_n^{-1/n}.$$  \hspace{1cm} (2)

Strong constraints on $E_{LIV}^{(n)}$ have been set in astroparticle physics by several techniques [18, 29, 39–46], and below we further constrain it with HAWC observations.

Photon decays. – Kinematically forbidden processes in classical relativity can be allowed in LIV scenarios, such

$\footnote{Hereafter, natural units are used, $c = \hbar = 1$.}$
as vacuum Cherenkov radiation, spontaneous photon emission, photon decay, and photon splitting [12, 28, 30–32, 47]. The last two could have strong effects on astrophysical photons due to the long distances and the VHE of those processes. Here we consider decay into both $e^+e^-$, and into multiple gamma rays.

Considering the photon decay, $\gamma \rightarrow e^+e^-$, due to superluminal LIV, the resulting decay rates are fast and effective at energies where the process is allowed [12, 48, 49]. This creates a hard cutoff in the gamma-ray spectrum with no high-energy photons reaching the Earth from cosmological distances above a given threshold. The threshold for any order $n$ is given by

$$\alpha_n \leq \frac{4m_e^2}{E_{\gamma}^n(E_{\gamma} - 4m_e^2)},$$

where $m_e$ stands for the electron mass [12]. Eqs. (2) and (3) show that the lower limits on $E_{\gamma}^{(n)}$ (upper limits on $\alpha_n$) become more stringent with the increase in the observed photon energy by a factor of $E_{\gamma}^{1+2/n} (E_{\gamma}^{n+2})$ for upper limits on $\alpha_n$.

From Eqs. (2) and (3), we can find $E_{\gamma}^{(n)}$ for $n = 1$ and 2,

$$E_{\gamma}^{(1)} \gtrsim 9.57 \times 10^{23} \text{eV} \left(\frac{E_{\gamma}}{\text{TeV}}\right)^{3},$$

$$E_{\gamma}^{(2)} \gtrsim 9.78 \times 10^{17} \text{eV} \left(\frac{E_{\gamma}}{\text{TeV}}\right)^{2}.$$  

Hence, a lower limit for $E_{\gamma}^{(n)}$. in the photon sector directly emerges from any observed high energy cosmic photon event. Different fermion decay channels can be explored, but only the lightest $\gamma \rightarrow e^+e^-$ channel is considered in this paper. Photon decay in flight from the source leads to a straightforward way to bound LIV that depends primarily on the highest energy photons observed, and secondarily on the energy resolution and uncertainties of the detector.

A second superluminal LIV decay process considered in this work is photon splitting to multiple photons, $\gamma \rightarrow N\gamma$. Refs. [19, 28] show that the dominant splitting process is the photon decay into three photons ($3\gamma$), which has been studied in a model of quantum electrodynamics including LIV and $n=2$.

The decay rate of photon splitting is [19, 20, 28]

$$\Gamma_{\gamma \rightarrow 3\gamma} = 5 \times 10^{-14} \frac{E_{\gamma}^{19}}{m_e^3 E_{\gamma}^{(2)} TeV^{10}},$$

which is significantly smaller than the photon decay rate considered in the previous section. However, this process has no threshold, and is kinematically allowed whenever $E_{\gamma} > p_{\gamma}^2$. It becomes significant when photons propagate through cosmological distances and also predicts a
cutoff at the highest energy part of the photon spectra of astrophysical sources. Despite the lack of a kinematical energy threshold, the strong photon energy dependence of Eq. (6) produces an effective one: an energy region narrow compared to HAWC’s energy resolution in which the probability for photons to arrive from a source sharply drops.

Because we observe photons from distant sources, we equate the mean free path of a photon to the distance between the source and observer, $L$, that is we take $L \Gamma = 1$, with $\Gamma$ translated to units of $\text{km}^{-1}$. The corresponding LIV limit, as a function of the highest photon energy, is given by,

$$E_{\gamma}^{(2)} > 3.33 \times 10^{19} \text{eV} \left(\frac{L}{\text{km}}\right)^{0.1} \left(\frac{E_{\gamma}}{\text{TeV}}\right)^{1.9}.$$  

Once again, this photon decay in flight from the source leads to a direct way to bound the LIV energy scale that mainly depends on the highest energy photons observed. It is interesting to note that the higher-order process of Eq. (7) produces a stronger limit than the lower order photon decay of Eq. (5).

Refs. [19, 20, 28] discuss a different method of setting limits on subluminal LIV with $n = 2$ using modifications to the Bethe-Heitler interaction of photons in the atmosphere. However, unlike the photon splitting process, this does not result in a sharp effective threshold. Thus setting a limit using this effect must use different analysis techniques than the ones we have used to analyze the HAWC data, and we must defer such analysis to a later publication.

Limit Calculation. – Since the emphasis here is on the upper extremes of the spectrum, several details of the HAWC analysis are changed compared to previous analyses such as that of the Crab Nebula spectrum [21]. First, we concentrate on the NN energy estimator as it is expected to have better energy resolution (1–1.5 in log$_{10}$ E/TeV above 50 TeV) [21]. Second, we re-bin the two highest bins of estimated energy, subdividing both the (100, 178) and the (178, 316) TeV bins into three finer bins each of equal size in log space.

We consider the Crab and other three other sources which have evidence of emission above 100 TeV in reconstructed energy [22, 50]. For spectral assumptions, we consider a log-parabola for the Crab, eHWC J1907+063, and eHWC J2019+368, and a cutoff-exponential model for eHWC J1825-134, as shown in Fig. 1. These choices are consistent with the more detailed information on the sources found in [21, 22]. In analogy with [22], we use the best-fit source position for reconstructed NN energy $> 56$ TeV. Finally, to desensitize the results to imperfect modeling of the point spread function, the analysis is carried out in bins with fixed radius about the central position (top hat bin), chosen for each source to be large enough that the results no longer depend on the choice of top hat radius; see the Supplemental Material [51].
This analysis provides a lower energy limit, $E_c$, beyond which there is weak or no evidence for the continuation of emission for each source. This lower limit on a hard cutoff also serves as an upper limit on observed photon energy, $E_{\gamma}$. We perform a fit to the chosen energy spectrum shape and compare the fit likelihood with that of the fit of an energy spectrum convolved with a hard cutoff at energy $E_c$. The hard cutoff is convolved with both the HAWC energy resolution and an additional smoothing of 0.1 in $\log_{10}(E/\text{TeV})$ width to avoid bin edge effects [51]. The smoothed hard cutoff is therefore wider than the actual HAWC energy resolution. Because the hard cutoff model accounts for photons which are mis-reconstructed with energy higher than $E_c$, this test is independent of any assumed spectral shape above $E_c$. Comparisons of the best-fit spectra with those expected with a hard cutoff at 100 TeV are shown in Fig. 1. The source spectra are discussed in detail in [21].

First, we consider whether sources show an actual preference for such a hard cutoff. Specifically, we find the profile likelihood (with spectral fit parameters optimized for each $E_c$) as a function of $E_c$ and consider the statistical significance of each value of $E_c$; see [51]. The statistical test is to calculate the log-likelihood ratio (details in [51]) of the fit with no cutoff and the fit including such a cutoff,

$$D = 2\ln\left(\frac{\mathcal{L}(\hat{E}_c)}{\mathcal{L}(\hat{E}_c \to \infty)}\right),$$

where $\hat{E}_c$ is the best fit value of $E_c$, and the null hypothesis is the LI limit $\hat{E}_c \to \infty$. We calculate the p-value of observing $D$ or greater (50% of D values are 0 since upward fluctuations can’t drive $E_c$ above $\infty$ [52]). The resulting p-values in the Table I indicate that none of the sources prefer a cutoff. Details of the binned likelihood and treatment of background and forward folding for resolution effects are given in [51].

Because our spectra do not indicate a significant preference for $E_c < \infty$, we proceed to set a lower limit on $E_c$, which would occur in LIV photon decay signatures. We consider here two confidence levels (CL): 95% and 99.73% (“3σ”). The corresponding values of $2 \Delta \ln \mathcal{L}$ (using Wilks’ theorem) for the intervals are 2.71, and 7.74. These limits are intrinsically one-sided, as we lose statistical power to identify a finite $E_c$ for large values of $E_c$. The results shown in Table I indicate that we have evidence for greater than 100 TeV emission at $>95\%$ CL from all four sources and $3\sigma$ evidence from three of them. More statistical detail can be found in [51].

The 95% CL limits are reinterpreted as limits on $E_c$. Then, by using Eqs. (4), (5), and (7) directly lead to lower limits to $E_{LIV}^{(1)}$ and $E_{LIV}^{(2)}$, while we derive upper limits on $\alpha_0$ from Eq. (3), when $n = 0$. Because a hard photon decay cutoff due to LIV would be at the same energy for any source, we also combined the likelihood profiles of all four sources and found an $E_c$ limit of 285 TeV, some 11% higher than the limit from eHWC J1825-134 alone [51].

In this way, HAWC can exclude the LIV energy scale of the new physics, $E_{LIV}^{(1)}$, to greater than $10^{31}\text{eV}$, over 1800 times the Planck energy scale ($E_{Pl} \approx 1.22 \times 10^{28}\text{eV}$), and more constraining than the best previous values [12, 29]. We calculate limits on $E_{LIV}^{(2)}$ from photon splitting only for individual sources, because the limit depends on the source distance to the observer [53]. These limits are more powerful than the $E_{LIV}^{(2)}$ limits from photon decay and more constraining than previous values [19, 20].

We present the HAWC 95% CL LIV limits in Table II. For comparison, Fig. 2 shows previous strong limits on photon decay using VHE photons from HEGRA telescope [12, 29], CANGAROO [17], and HESS [15]. We also show limits due to LIV energy-dependent time delay searches with the Fermi-LAT [18], and limits due to photon splitting [19, 20]. For a more comprehensive list of these limits and those presented in this work including corresponding values of $\alpha_n$, see the Supplemental Material [51].

We derived the limits above for the LIV coefficients within the general MDR framework, although related limits can also be evaluated in the framework of the Standard Model Extension (SME) [11, 54]. The SME provides a general field-theoretic framework that consid-

| Source         | p-value $E_c(95\%)$ | $E_c(3\sigma)$ |
|----------------|---------------------|----------------|
| eHWC J1825-134 | 1.000               | 244            |
| eHWC J1907+063 | 0.990               | 218            |
| eHWC J0534+220 | 1.000               | 152            |
| eHWC J2019+368 | 0.828               | 120            |

Table I. HAWC sources and Photon Energy Limits (TeV).
Table II. HAWC sources and 95% CL lower limits on $E_c$, LIV coefficients, and the distance to the observer, $L_c$, $\alpha_0$ are upper limits while $E_{LIV}^{(n)}$ are lower limits. Systematic uncertainties are given in the Supplemental Material [51].

| Source          | $E_c$ | $L$ | $\alpha_0$ | $E_{LIV}^{(1)}$ | $E_{LIV}^{(2)}$ | $E_{LIV}^{(3)}$ |
|-----------------|------|----|-----------|----------------|----------------|----------------|
|                | TeV  | kpc| $10^{-17}$| $10^{31}$ eV | $10^{33}$ eV | $10^{35}$ eV   |
| J1825-134       | 244  | 1.55| 1.75      | 1.39           | 0.58           | 12             |
| J1907+063       | 218  | 2.37| 2.2       | 0.99           | 0.47           | 10.1           |
| J0534+220       | 152  | 2   | 4.52      | 0.34           | 0.23           | 4.99           |
| J2019+368       | 120  | 1.8 | 7.25      | 0.17           | 0.14           | 3.15           |
| Combined        | 285  | -   | 1.29      | 2.22           | 0.8            | -              |

Figure 2. HAWC 95% CL LIV limits for $n = 0$, 1 and 2. We show previous strong constraints due to photon decay, as well as based on an energy-dependent time delay ($\Delta t_{LIV}$) and photon splitting ($3\gamma$). For $n = 1$, HAWC limits are orders of magnitude above $E_{\gamma_1} \approx 10^{28}$ eV.

Table III. Effects of systematic errors on $E_c$ for combined sources.

| Source DESCRIPTION | EFFECTS |
|--------------------|---------|
| Simulation         | -4% to +7% |
| Spectrum choice    | -1%     |
| Source location    | -1%     |
| Energy scale       | -6%     |
| Overall            | -7% to +7% |

**Conclusion.** - The HAWC Observatory measurements of the highest-energy photons can be used to probe fundamental physics such as violation of Lorentz invariance.
In this work, we set LIV limits by searching for LIV photon decays through the study of four sources with significant high energy emission, including the Crab Nebula. We found that none of them favor a spectrum with a hard cutoff and HAWC finds evidence of 100 TeV photon emission at 95% CL from four astrophysical sources, with 3σ evidence from three of them. Furthermore, the dedicated search for such a signature in the spectra increases the energy to which the existence of the most energetic photons can be confirmed, which leads to the new and stringent limits on LIV in Table II, showing an improvement over previous limits of 1-2 orders of magnitude.

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