Recovering stellar population parameters via different population models and stellar libraries

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ABSTRACT
Three basic ingredients are required to generate a simple stellar population (SSP) library, i.e. an initial mass function (IMF), a stellar evolution model/isochrones, and an empirical/theoretical stellar spectral library. However, there are still some uncertainties to the determination and understanding of these ingredients. We perform the spectral fitting to test the relative parameter offsets between these uncertainties using two different stellar population models, two different empirical stellar libraries, two different isochrones, and the Salpeter and Chabrier IMFs. Based on these setups, we select five SSP libraries generated with the Galaxev/STELIB and Vazdekis/MILES models, and apply them to the pPXF full-spectrum fitting of both MaNGA and mock spectra. We find that: (1) Compared to the Galaxev/STELIB model, spectral fitting qualities with the Vazdekis/MILES model have significant improvements for those metal-rich (especially oversolar) spectra, which cause better reduced \(\chi^2\) distributions and more precisely fitted absorption lines. This might due to the lack of metal-rich stars in the empirical STELIB library, or code improvement of the Vazdekis model. (2) When applying the Vazdekis/MILES model for spectral fitting, the IMF variation will lead to not only a systematic offset in \(M_*/L_r\), but also offsets in age and metallicity, and these offsets increase with increasing stellar population ages. However, the IMF variation caused metallicity offsets disappear in the case of Galaxev/STELIB based libraries. (3) The Padova2000 model provides a better match to the MaNGA galaxy spectra at \([M/H]<-1.0\), while the BaSTI model match the local galaxy spectra better at \([M/H]>-1.0\). Current tests suggest that spectral fitting with the Vazdekis/MILES + BaSTI combination would be a better choice for local galaxies.

Key words: galaxies: evolution – galaxies: fundamental parameters.

1 INTRODUCTION

Galaxy formation and evolution processes can partly be resolved by analysing their stellar population properties, e.g. star formation history (SFH), stellar mass, age, metallicity and abundance pattern, dust extinction, and gas fraction (see a review by Conroy 2013). However, many of these population parameters are encoded together and need to be decomposed. One way of the decomposition is by stellar population synthesis modelling (Tinsley 1968), which is initially developed at a certain age and metallicity (e.g. Tinsley 1968; Searle, Sargent & Bagnuolo 1973; Tinsley & Gunn 1976; Bruzual 1983), and then improved to the whole age and metallicity parameter spaces (Charlot & Bruzual 1991; Bruzual & Charlot 1993; Bressan, Chiosi & Fagotto 1994; Worthey 1994; Fioc & Rocca-Volmerange 1997; Maraston 1998; Leitherer et al. 1999; Vazdekis 1999; Walcher et al. 2011).

Based on the stellar population synthesis modelling, one can produce a single stellar population (SSP) library by assuming a certain initial mass function (IMF), a stellar evolution model/isochrones, and an empirical stellar spectral library. Together with an SFH, chemical evolution, and dust attenuation and emission model to the SSP library, one can then construct composite stellar population (CSP) templates.

For the three ingredients required for generating an SSP library, i.e. IMF, isochrones, and empirical stellar spectral library, many efforts have been dedicated to their measurements or improvements. The IMF was initially described with the form \(dN/dM \propto M^{-\alpha}\) with \(\alpha = 2.35\) (Salpeter 1955). According to the measurements from solar neighbourhood, the form deviates from the Salpeter form only at
with a lognormal or shallower power law (Kroupa 2001; Chabrier 2003). Historically no strong IMF variation evidence is found before 2010 (e.g. Bell & de Jong 2001; Bastian, Covey & Meyer 2010). Since then, different methods are proposed and the derived results support a non-universal IMF at the low-mass end (see a review by Cappellari 2016). Evidence is obtained mainly in three ways: (1) gravitational lenses combined with dynamical modelling (e.g. Auger et al. 2010; Treu et al. 2010; Posacki et al. 2015) or spatially resolved galaxy kinematics and dynamics (e.g. Cappellari et al. 2012; Lasker et al. 2013; Tortora et al. 2013; Posacki et al. 2015; Li et al. 2017); (2) analyses of IMF-sensitive absorption-line indicators based on stellar population modelling (van Dokkum & Conroy 2010; Conroy & van Dokkum 2012; Spiniello et al. 2012; La Barbera et al. 2013; Spiniello, Trager & Koopmans 2015; La Barbera et al. 2016; Zielensiewski 2017; Parikh et al. 2018; Vaughan et al. 2018; Zhou et al. 2018).

A number of public isochrone tables are now available (e.g. Schaller et al. 1992; Bertelli et al. 1994; Cassisi et al. 2000; Girardi et al. 2000; Yi et al. 2001; Cioni et al. 2006; Dotter et al. 2007). The calculation of isochrones from different groups focus on different aspects of stellar evolution (see the summary by Conroy 2013). The Geneva models (Schaller et al. 1992; Meynet & Maeder 2000) trace the evolution of high-mass stars well but has no isochrones for low-mass stars. The Y^2 models (Yi et al. 2001; Yi, Kim & Demarque 2003), the Dartmouth models (Dotter et al. 2008), and the Victoria-Regina models (Vandenberg & Bell 1985; Vandenberg, Bergbusch & Dowler 2006) focus on the evolution of stars in the main sequence, red giant, and horizontal branches. The Lyon models (Chabrier & Baraffe 1997; Baraffe et al. 1998) are widely used in tracing isochrones of very low mass stars and brown dwarfs. The most popular models can span a wide range in ages, metallicities, and evolutionary phases. These include the Padova (Bertelli et al. 1994; Girardi et al. 2000; Marigo et al. 2008) and BaSTI (Pietrinferni et al. 2004; Cordier et al. 2007; Hidalgo et al. 2018) models.

The third ingredient for producing an SSP library is stellar spectral library, which includes both theoretical ones, such as the BaSel library (Lejeune, Cuisinier & Buser 1997, 1998; Westera et al. 2002), and empirical ones, including Gunn & Stryker (1983), Pickles (1998), Jones (1999), ELODIE (Pruziel & Soubiran 2001), STELIB (Le Borgne et al. 2003), Indo-US (Valdes et al. 2004), GRANADA (Martins et al. 2005), NGSX (Gregg et al. 2006; Heap & Lindler 2011), MILES (Sanchez-Blazquez et al. 2006), IRTF (Rayner et al. 2009), and the X-shooter library (Chen et al. 2011).

With different combinations of the above three ingredients, there are many public SSP libraries available, such as BC03 (Bruzual & Charlot 2003), M05 (Maraston 2005), FSPS (Conroy, Gunn & White 2009), Vazdekis/MILES (Vazdekis et al. 2010), and M11 (Maraston & Stromback 2011).

Many works have been devoted to identify the advantage and weakness of different SSP libraries. Koleva et al. (2008) compared the BC03 and Vazdekis/MILES SSP libraries by concentrating on old population of Galactic globular clusters, and found that BC03 library had systematic biases at non-solar metallicity, which might be due to the poor metallicity coverage of the STELIB empirical stellar spectral library. Conroy & Gunn (2010) applied BC03, M05, and FSPS SSP libraries to multiband photometric data, and summarized that these libraries had different performance in different comparison cases. Gonzales Delgado & Cid Fernandes (2010) applied different combinations of isochrones and empirical stellar libraries to full-spectrum fitting of star clusters, and concluded that the BC03 library may underestimate metallicity by as much as 0.6 dex, and overestimate extinction by 0.1 mag. If one uses the SSP library with MILES and GRANADA empirical stellar spectral library, the fitting accuracies could be improved by 0.1 dex in age and 0.3 dex in metallicity. Chen et al. (2010) analysed full-spectrum fitting results of SDSS galaxies in different types, and derived significant difference when applying different SSP libraries using the STARLIGHT fitting.

Star clusters or globular clusters, which (mostly) have a single age and single metallicity, are considered as good targets for validation of SSP libraries. When observing galaxies with an integral field unit (IFU) instrument, we can spatially resolve them and obtain spectra at different radii. Those spatially resolved spectra from different types of galaxies, which actually include many galaxy evolutionary phases and cover a wide range of ages and metallicities, can also be used for validating the advantage and disadvantage of different SSP libraries.

Over the past two decades, many IFU surveys are designed based on different scientific goals. There are six IFU surveys focusing on a certain type of galaxies. The SAURON (de Zeeuw et al. 2002) and ATLAS13 (Cappellari et al. 2011) performed IFU survey of local elliptical and lenticular galaxies. The DiskMass Survey (Bershady et al. 2016) targets 146 face-on star-forming galaxies at high spectral resolution (R ∼ 10 000). The VENGA survey (Blanc et al. 2013) points to 30 nearby spiral galaxies with high spatial resolution and deep observations. The SLUGGS Survey (Brodie et al. 2014) focuses on 25 nearby early-type galaxies with large spatial coverage (reach to ~8 Re). The MASSIVE Survey (Ma et al. 2014) observes ~100 most massive (stellar mass $M_\star > 10^{11.5} M_\odot$) galaxies within 108 Mpc. There are also three surveys targeting all types of galaxies. The CALIFA survey (Sanchez et al. 2012) has already finished their ~600 galaxy survey with two sets of wavelength coverages and spectral resolution: V500 (3745–7500 Å, R = 850) and V1200 (3400–4840 Å, $R = 1650$). The SAMI survey (Croom et al. 2012) will observe 3400 galaxies with two wavelength channels (3700–5700 and 6250–7350 Å). The largest of all, the SDSS IV/ManGA survey (Bundy et al. 2015) aims to observe 10 000 galaxies by covering 10$^3 M_\odot < M_\star < 10^{11} M_\odot$ and redshift $z < 0.15$ with spectral resolution R ∼ 2000 and a wide wavelength coverage 3600–10300 Å.

With these IFU data, we can make further progress on the understanding of galaxy evolution. However, to extract stellar population parameters, one has a bewildering number of options in the SSPs, and is pressed to understand the relative strengths and weaknesses in different routines.

In Ge et al. (2018), we studied the spectral fitting biases and scatters of two full-spectrum fitting algorithms, pPXF and STARLIGHT, in the absence of any model uncertainties. We found that pPXF gave stellar population parameters with smaller biases and scatters than STARLIGHT. We also presented the relationships between parameter biases (or scatters) and the signal-to-noise ratio of the spectra. By dividing the population parameter results into different metallicity bins and presenting population parameters at different ages, we explained the fitting biases and scatters more clearly than using the real data.

With the clear interpretation of algorithm-induced biases and scatters, we are going to analyse how the resulting population parameters will be affected by the assumptions of stellar evolution model, IMF, and stellar spectral library through both simulations.
and observations. In this paper, we focus on fitting offsets derived from different SSP libraries, by dividing the measured luminosity-weighted metallicities into different bins, then present the parameter difference caused by different SSP libraries based on both observation and simulation.

We will select the full-spectrum fitting code and SSP libraries, and describe our spectral fitting procedures in Section 2. In Section 3, we analyse the SDSS-IV/MaNGA data with our selected SSP libraries, and compare the relative parameter offsets induced by the two choices of each ingredient. To have a direct judgement on which model is closer to the reality, we do the same analyses with simulation to interpret the origin of these relative offsets. We discuss the scatter of our results, and also compare them with previous works in Section 4. The conclusion is made in Section 5, in which we also give recommendation on how to select these ingredients for real spectral fitting.

2 PREPARATION FOR MODEL UNCERTAINTY TESTS

2.1 Full-spectrum fitting code: pPXF

Ge et al. (2018) have performed a systematic analysis on the algorithm bias and scatter of both pPXF (Cappellari & Emsellem 2004; Cappellari 2017) and STARLIGHT (Cid Fernandes et al. 2005) full-spectrum fitting codes, and found that pPXF can recover stellar population parameters better than STARLIGHT and have almost no parameter biases on dust extinction and error spectrum types. More recently, Cid Fernandes (2018) showed that the convergence of STARLIGHT can be improved with a different choice of the Markov Chain initialization in the code. But this sensitivity to the initial conditions confirms its intrinsic weakness. In any case, even at comparable accuracy, Ge et al. (2018) found pPXF to be two to three orders of magnitude faster than STARLIGHT, and this alone would justify our choice of pPXF in this paper. Therefore, in this work, we apply pPXF (PYTHON version V6.7.6) for model uncertainty tests.

2.2 Empirical stellar spectral libraries

As is compared by Vazdekis et al. (2010), the STELIB empirical stellar spectral library shows almost the poorest coverage of fundamental parameter space, while the MILES library is the richest one. To have a thorough analysis on the effect of model uncertainties caused by empirical stellar spectral library, we select STELIB and MILES libraries for comparisons. In principle, the one with more stars should represent the real case better.

The STELIB library includes 245 stellar spectra with wavelength range 3200–9500 Å and spectral resolution R ∼ 2000 (Le Borgne et al. 2003). This library has a shortage of hot (>10 000 K), metal-rich, and cool dwarf stars.

The MILES library contains 985 stars with wavelength coverage from 3500 to 7500 Å and spectral resolution FWHM = 2.3 Å (Sanchez-Blazquez et al. 2006). Compared to STELIB library, the MILES library improved the range of metallicity.

1Here we use the word ‘offset’ to describe those parameter differences fitted with different SSP libraries, since we do not know which one is true. While we use ‘bias’ to describe the difference between the fitted parameter and its true value, e.g. simulations in Appendix A3.

2Available from http://purl.org/cappellari/software

2.3 IMF selection

Currently, there are mainly three kinds of IMFs calibrated based on the stellar observations of our Milky Way: Salpeter, Kroupa, and Chabrier (Fig. 1 left). The Salpeter IMF is a power law, while the Kroupa and Chabrier IMFs reduce the contribution of low-mass stars (m∗ < 1 M⊙) at different levels. The Salpeter IMF has the largest fraction of low-mass stars, leading to the largest M/L ratio in the optical at a certain age and metallicity among the three IMFs. While the Chabrier IMF yields the smallest M/L. We hence select the Salpeter and Chabrier IMFs for analyses. The results for the Kroupa IMF would be in between.

The integrated stellar mass difference between the Salpeter and Chabrier IMFs as a function of upper mass limit is shown in the middle panel of Fig. 1. With stellar evolution, high-mass stars explode first, hence the total mass difference between the two IMFs increases with decreasing upper mass limit. Here we only calculate the mass of stars without including the mass-loss from stellar wind, and also exclude the mass contribution from stellar remnants, including white dwarfs, neutron stars, and black holes.

At the beginning of stellar evolution, the integrated stellar mass of the Chabrier IMF is 0.15 dex lower than that of Salpeter’s IMF. The integrated mass difference then increases with time, due to the decreased fraction of high-mass stars. However, when we calculate the M/L, the M∗ contains not only living stars, but also stellar remnants. Therefore, the M/L difference caused by the two IMFs will not decrease as steep as shown in the middle panel of Fig. 1. For all the calculations in our work, the M/L means M∗ + remnants/L.

After taking the stellar remnants into account, the M/L will not simply decrease along the stellar evolution time, but have a turnover after 3 Gyr (the right-hand panel of Fig. 1). The trends of the M/L versus stellar evolution time depend on different stellar evolution isochrones and stellar population synthesis models.

2.4 Stellar evolutionary isochrones

From the literature, we can find many public isochrones. However, different models focus on different stellar evolutionary processes. If one wants to apply those SSP libraries to local galaxies, which include both old and young, metal-poor and metal-rich stars, we need to select those isochrones that can cover a wide range of stellar ages, metallicities, and evolutionary phases. We thus select the widely used Padova2000 (Girardi et al. 2000; Marigo et al. 2008) and BaSTI (Pietrinferni et al. 2004; Cordier et al. 2007) evolutionary isochrones for comparison.

Both the Padova and BaSTI groups track the stellar evolution from the main sequence to thermally pulsating asymptotic giant branch states, but their treatments of the thermally pulsating asymptotic giant branch phase are very different. A detailed comparison of these two isochrones is shown in the fig. 1 of Conroy & Gunn (2010).

2.5 SSP libraries: Galaxev/STELIB and Vazdekis/MILES

Our analyses on model uncertainties mainly focus on comparing the relative parameter offsets, \( \Delta P = P_{\text{LibA}} - P_{\text{LibB}} \), where \( P_{\text{LibA}} \) and \( P_{\text{LibB}} \) correspond to the stellar population parameters derived from the pPXF fitting with two different SSP libraries, respectively. For
The Salpeter (black colour), Kroupa (blue colour), and Chabrier (red colour) IMFs are shown in the left-hand panel. With the stellar evolution, high-mass stars explode more and more, and the $M_*/L$ difference between the Salpeter and Chabrier IMFs becomes larger. The middle panel shows the integrated stellar mass (integrating from $0.1 \, M_\odot$ to the upper limit) difference between the Chabrier and Salpeter IMFs. The right-hand panel presents the $\Delta M_*/L_*$ between Chabrier and Salpeter IMFs along the stellar evolution time for Vazdekis/MILES (plus symbols) and Galaxev/STELIB (cross symbols) models, respectively.

**Table 1.** Five SSP libraries with different combinations of ingredients.

| SSP library | Model          | IMF   | Isochrone |
|-------------|----------------|-------|-----------|
| Lib1        | Vazdekis/MILES | SALP  | P00       |
| Lib2        | Vazdekis/MILES | CHAB  | P00       |
| Lib3        | Vazdekis/MILES | SALP  | BaSTI     |
| Lib4        | Galaxev/STELIB | SALP  | P00       |
| Lib5        | Galaxev/STELIB | CHAB  | P00       |

Note. Here the SALP is for Salpeter, the CHAB is for Chabrier, and P00 is for Padova2000.

each ingredient required for constructing an SSP library, we will check the parameter offsets caused by its variation.

To compare the two assumptions for each ingredient (the Salpeter and Chabrier IMFs, the MILES and STELIB stellar spectral libraries, the BaSTI and Padova stellar evolutionary isochrones), Bruzual & Charlot (2003) and Vazdekis et al. (2010) provide matched SSP libraries for our tests.3 We then select the Galaxev/STELIB and Vazdekis/MILES model based SSP libraries for observational and simulation analyses. The five SSP libraries listed in Table 1 are finally selected with different combinations of the three ingredients, by which we can perform our analyses on relative parameter offsets caused by the variation of each ingredient.

Since the empirical MILES library contains more stars and covers more thorough fundamental parameter space than STELIB, we also adopt the Vazdekis (Vazdekis et al. 2010) model with empirical MILES library (Vazdekis/MILES) to check the model effects of varied IMFs and isochrones. As shown in Table 1, Lib1 and Lib2 can be used for checking the parameter offsets caused by the Salpeter and Chabrier IMFs, while Lib1 and Lib3 are selected for checking the difference between the Padova and BaSTI isochrones. To identify the effect of different empirical libraries, we take Lib1 and Lib4 for comparison, where Lib4 is generated based on the Galaxev (Bruzual & Charlot 2003) evolutionary model with empirical STELIB library (Galaxev/STELIB). In this comparison we assume the Padova isochrone and Salpeter IMF as Lib4 for comparing the empirical MILES and STELIB libraries. Here we also select Lib5 with the combination of Galaxev/STELIB + Padova isochrone + Chabrier IMF for a double-check of IMF effects. Both the Salpeter and Chabrier IMFs assumed in the Vazdekis/MILES and Galaxev/STELIB models have the same stellar mass range: $(0.1, 100) \, M_\odot$.

For both the Lib1 and Lib2 SSP libraries, we select six metallicities ([M/H] = $-1.71, -1.31, -0.71, -0.4, 0.0, 0.22$) and a subset of 25 logarithmically spaced equally sampled ages between 0.06 and 15.85 Gyr. For Lib3, which is based on the BaSTI model, the age and metallicity grids are different from that of Lib1 and Lib2. Therefore, we select those grids closest to the SSP ages and metallicities selected above, respectively. The metallicity grids are [M/H] = $-1.79, -1.26, -0.66, -0.35, 0.06, 0.26$. The age grids are $t/$Gyr = $0.06, 0.08, 0.09, 0.1, 0.15, 0.2, 0.25, 0.3, 0.4, 0.5, 0.6, 0.8, 1.0, 1.25, 1.5, 2.0, 2.5, 3.25, 4.0, 5.0, 6.5, 8.0, 10.0, 12.5, 14.0.

For Lib4 and Lib5, their metallicity grids are the same as Lib1 and Lib2, but the age grids have small difference. We hence select those age grids closest to that in Lib1 and Lib2 for tests.

Fig. 2 shows the parameter distributions of the stellar age versus $M_*/L_*$ for the five SSP libraries listed in Table 1. Different from the middle panel of Fig. 1, here the models do include the effects of mass-loss and stellar remnants. SSPs with the same age but higher metallicities usually have lower mass-loss rate and higher $M_*/L_*$ than that with lower metallicities. However, the $M_*/L_*$ increasing trend of the Lib1 and Lib2 libraries are different from the Lib3, Lib4, and Lib5 libraries. In the five panels of Fig. 2, for models with different metallicities, the Lib1 and Lib2 libraries give similar $M_*/L_*$ dependences on metallicities at different stellar ages. While the Lib3–Lib5 libraries tend to have smaller $M_*/L_*$ differences among different metallicities at young ages ($t < 10^9$ yr), but these differences increase towards older ages ($t > 10^9$ yr).

As shown in the right-hand panel of Fig. 1, the variation of $\Delta \log (M_*/L_*)$ along stellar evolution have the similar trends for both the Vazdekis/MILES (the plus symbols) and Galaxev/STELIB (the cross symbols) models when $t < 10^9$ yr or $M_{\text{Upper limit}} > 20 \, M_\odot$ (the middle panel of Figure 1). These variation trends are also consistent for different metallicities until $t > 10^9$ yr. Then the $M_*/L_*$ offset becomes smaller and those SSPs with poorest metallicity have the smallest offset. One important thing should be pointed out: although applying the same Salpeter and Chabrier IMFs for generating SSP libraries, the $\log (M_*/L_*)$ differences calculated by the Vazdekis/MILES model are $<0.05$ dex systematically smaller than those by the Galaxev/STELIB model. Even assuming the same stellar evolutionary isochrone and IMF for input, the $M_{\text{*, rem}}$ at the same age and metallicity given by the Vazdekis and Galaxev models are different. We have to keep this in mind when comparing the Lib1 and Lib4 libraries to study the model offsets caused by the empirical MILES and STELIB stellar spectral libraries.
The stellar age versus $M_*/L_r$ in six metallicities of the Lib1–Lib5 (from left-hand to right-hand panels) SSP libraries. In each panel, the stellar metallicities are shown in different colours: [M/H] = −1.71 (blue), −1.31 (cyan), −0.71 (green), −0.4 (black), 0.0 (violet), and 0.22 (red).

2.6 MaNGA data analysis

With the selected pPXF code and five SSP libraries, we can apply them to fit SDSS-IV/MaNGA spectra and identify parameter offsets caused by different model uncertainties. Considering current IFU observations have low S/N (<1) at large galaxy radii, we select only spaxels with S/N > 5 and spatially rebin them to reach S/N ~ 60 based on the Voronoi 2D binning method (Cappellari & Copin 2003). Here the S/N of each spaxel is defined by

$$S/N = \text{median} \left( \frac{F_{\lambda}}{\sigma_{\text{err},\lambda}} \right), \lambda = 5490–5510 \, \text{Å}.$$ (1)

For these spatially re-binned spectra, we perform the pPXF fitting by assuming a uniform CAL (Calzetti et al. 2000) dust reddening curve to correct the intrinsic dust extinction. This work aims to distinguish the effect of models choices using a state-of-the-art spectral fitting code with different SSP libraries and to estimate random uncertainties from ensembles of 50 Monte Carlo simulations. For the pPXF fits, we do not use regularization (we set ‘regul = 0’). This is because, while regularization is useful to reduce the effect of noise on a single fit to a single galaxy spectrum, by design it will reduce the scatter in Monte Carlo realization by making the fitted weights of all realizations look similar. For this reason, for a proper estimate of model uncertainties, regularization should not be used (see a similar discussion in section 3.4 of Cappellari & Emsellem 2004). In the spectral fitting, we also mask those emission lines as done in Ge et al. (2018). Although the pPXF code can fit emission lines together with the stellar population templates, which might improve the fitting quality especially for the Balmer lines, we choose to mask the emission lines as this can be applied equally to both the real data and the simulations. The simulations using combinations of SSPs based on the assumed lognormal SFH (see Appendix A for details) are needed to interpret the results derived from MaNGA data. Therefore, in this work, we mask emission-line regions in both the observed and the simulated spectra in exactly the same way.

When comparing different SSP libraries, the reduced $\chi^2$ is an effective parameter for finding out their differences. However, this value depends on the accuracy of flux uncertainty estimation. To avoid the over- or underestimation of flux uncertainty, we first use pPXF + Lib1 to fit a spectrum and obtain its best-fitting model. Then we can derive the spectral fitting residuals by subtracting the best-fitting model. The root mean square ($\sigma_{\text{resid}}$) is hence derived based on the spectral residuals. We finally use this $\sigma_{\text{resid}}$ to normalize the error spectrum as follows:

$$F_{\text{err},\lambda} = F_{\text{resid},\lambda} \times \frac{\sigma_{\text{resid}}}{\text{median}(F_{\text{err}})}.$$ (2)

With this normalization, we can (1) keep the shape of the error spectrum along wavelength, which reflects the instrumental dependence, and (2) avoid the possibly mis-estimated flux uncertainty.

The uncertainties of those fitted population parameters are estimated based on simulation. For each spectrum, we first use the pPXF code and selected SSP library to obtain the best-fitting model. Then we generate 50 mock spectra based on the best-fitting model and the corrected error spectrum by assuming the observed flux at each wavelength point follows a Gaussian distribution. After performing the same fitting procedure as done to the observed spectrum, we can derive the parameter uncertainties based on the 50 fitted values of each parameter.

Once we obtain the full-spectrum fitting results, we further divide these spectra into six metallicity bins (as shown in Fig. 2) based on their luminosity-weighted metallicities derived from pPXF + Lib1. In each metallicity bin, we identify each spectrum with SDSS $r$-band luminosity-weighted age. With these two steps, we can then perform detailed analyses of parameter offsets caused by different model uncertainties.

3 RESULTS

The effects of model uncertainties can be reflected by different metrics. The reduced $\chi^2$ of full-spectrum fitting shows the fitting quality directly, from which we can compare different model assumptions. For those ingredients that cannot be differentiated by the reduced $\chi^2$ distributions, we analyse their fitting offsets and scatters by a series of comparisons, and finally provide a judgment on how suitable they are at fitting different types of galaxies.

3.1 $\chi^2$ comparisons: the dominant effect of full-spectrum fitting quality

To compare the fitting quality of different models, we randomly select 100 MaNGA galaxies observed with the 127-fiber bundle, which include 26 elliptical and 74 spiral galaxies as classified by the Galaxy Zoo project (Willett et al. 2013). Those spectra with low S/N (5 < S/N < 60) are spatially re-binned to S/N ~ 60 by the Voronoi 2D binning method (Cappellari & Copin 2003), which make sure all the spectra we applied for full-spectrum fitting have
DOF is the degree of freedom of each spectrum. Fitting results based on Delta1 >= 0.1 dex (See Appendix A3). Based on this, we thus apply the pPXF ingredients. From this, we try to identify the dominant ingredient + SALP Vazdekis/MILES-based SSP libraries: Lib1 (Vazdekis/MILES + CHAB + P00, red colour) and Lib3 (Vazdekis/MILES + CHAB + P00, red colour), and Lib3 corresponds to Vazdekis/MILES model + Salpeter IMF + Padova2000 isochrone (light green colour). The reduced χ^2 distributions derived from the Galaxev/STELIB model are shown in green or light green colours. Here Lib4 defines the combination of Galaxev/STELIB + Salpeter IMF + Padova2000 isochrone (green colour) and Lib5 defines that of Galaxev/STELIB + Chabrier IMF + Padova2000 isochrone (light green colour). sufficiently high S/N. There are ~6000 spatially re-binned spectra in total, sampled at different galaxy radii.

When fitting the observed spectra, the measured parameter biases include: (1) algorithm bias, (2) S/N effect, and (3) model bias. From our test in Ge et al. (2018), there are almost no algorithm bias caused by the pPXF code at very high S/N (e.g. 300). At S/N = 60, the biases and scatter of age, metallicity and M/L are all less than 0.1 dex (See Appendix A3). Based on this, we thus apply the pPXF code to fit those MaNGA spectra with S/N >= 60, and then compare the relative parameter offsets (∆P) derived from different model assumptions. For those relative offsets larger than 0.1 dex, they should be caused by model uncertainties, instead of any algorithm bias or S/N effect.

We start from comparing the reduced χ^2 distribution of full-spectrum fitting based on different combinations of the three ingredients. From this, we try to identify the dominant ingredient for improving the fitting quality in the current set-up of SSP libraries.

Fig. 3 shows the reduced χ^2 distribution from the fitting of 100 MaNGA galaxies. Here the reduced χ^2 is defined as χ^2/DOF, where DOF is the degree of freedom of each spectrum. Fitting results based on different SSP libraries are divided into two groups:

(i) The reduced χ^2 distributions derived from three Vazdekis/MILES-based SSP libraries: Lib1 (Vazdekis/MILES + SALP + P00, blue colour), Lib2 (Vazdekis/MILES + CHAB + P00, red colour), and Lib3 (Vazdekis/MILES + CHAB + P00, violet colour).

(ii) The reduced χ^2 distributions derived from two Galaxev/STELIB-based SSP libraries: Lib4 (Galaxev/STELIB + SALP + P00, green colour) and Lib5 (Galaxev/STELIB + CHAB + P00, light green colour).

The five reduced χ^2 distributions shown in Fig. 3 provide us the following information:

(1) The Vazdekis/MILES model based SSP libraries (Lib1–Lib3) provide significant improvement on the fitting quality (coloured lines in the left-hand panel) compared to Galaxev/STELIB based ones (Lib4 and Lib5). As we can see, the reduced χ^2 distribution with the STELIB library shows a decrease in the peak around χ^2/DOF ~ 1 and an extra tail at large χ^2/DOF ≥ 1.2.

(2) Different IMF assumptions show little effects to the reduced χ^2 distribution (Lib1 versus Lib2, and Lib4 versus Lib5).

(3) The selection of isochrones also show little effects to the fitting quality (Lib1 versus Lib3).

From Fig. 3, we can only see a significant fitting improvement by Vazdekis/MILES model based libraries, but the reason of this improvement requires further clarification. Based on the luminosity-weighted stellar ages and metallicities derived from pPXF + Lib1, we further divide each χ^2 distribution into six metallicity bins and three age bins, by which we attempt to identify the detailed fitting quality in each bin and find out the detailed difference caused by the Lib1–Lib5 libraries.

In Fig. 4, the reduced χ^2 distributions fitted with Lib1–Lib5 libraries are shown in the top to bottom rows, respectively. Spectra with poor to rich metallicities are shown from the left to right columns. We also divide stellar ages into young (tL < 3 Gyr, green colour), and old (tL > 3 Gyr, red colour) age bins to track the possible evolution variation.

Those reduced χ^2 distributions obtained from the three Vazdekis/MILES SSP libraries (Lib1 in the first row to Lib3 in the third row) show no obvious difference at each metallicity and age bin. The results fitted with Galaxev/STELIB SSP libraries (Lib4 in the fourth row and Lib5 in the fifth row) are similar to that with Vazdekis/MILES ones at [M/H] ≤ −0.2 for both the young and old age bins. In the metal-rich cases ([M/H]L > −0.2), the reduced χ^2 from Lib4 to Lib5 are systematically larger than that from Lib1 to Lib3, which is reflected by median values of the two age bins (vertical dashed line). These median values present the largest differences (∆χ^2/DOF ~ 0.2) for those spectra with tL > 3 Gyr at the largest metallicity bin ([M/H]L > 0.1), and these differences are the same for both Lib4 and Lib5 reduced results. The green histograms in the [M/H]L > 0.1 bin only include eight spectra with stellar ages 1 Gyr < tL < 3 Gyr. Although their median values are similar, we cannot derive a robust statistical conclusion.

The above results might be explained as follows: (1) The STELIB library lacks metal-rich stars, but the MILES library includes sufficient such stars. SSP templates with supersolar metallicities are not well calibrated for Lib4 and Lib5 libraries, leading to larger reduced χ^2 than those derived from Lib1, Lib2, and Lib3 libraries. (2) The difference between Salpeter and Chabrier IMFs mainly happens to those low-mass stars (< 1 M⊙), which cause large mass difference but only have small light contribution. (3) The isochrones given by Padova2000 and BaSTI models are the same in most of the cases, their difference cannot be differentiated easily in the reduced χ^2 distributions.

Based on the above analyses of the reduced χ^2 distributions, we can only see some of the effects on how the choice of ingredients affect the fitting quality. How these stellar population parameters are biased by different choices of the three ingredients (IMF, isochrones, and empirical library) require further investigation.

3.2 Defining the relative parameter offset

Since the algorithm caused parameter biases and scatters of the pPXF code are all smaller than 0.1 dex at S/N ≥ 60 (Appendix A3), we can confirm the effects of model uncertainties if the correspond-
Comparison of different SSP libraries

Figure 4. The reduced $\chi^2$ distributions of the MaNGA full-spectrum fitting results based on Lib1–Lib5 SSP libraries. From top to bottom rows, we show the reduced $\chi^2$ distributions resulting from the fittings by using Lib1–Lib5. To match the input SSP metallicity range, we use the population parameters derived from pPXF + Lib1 to divide the fitted $[\text{M}/\text{H}]_L$ into six bins: $[\text{M}/\text{H}] < -1.5$ (Column 1), $-1.5 < [\text{M}/\text{H}] < -1.0$ (Column 2), $-1.0 < [\text{M}/\text{H}] < -0.5$ (Column 3), $-0.5 < [\text{M}/\text{H}] < -0.2$ (Column 4), $-0.2 < [\text{M}/\text{H}] < 0.1$ (Column 5), and $[\text{M}/\text{H}] > 0.1$ (Column 6). In each panel, the stellar ages derived from pPXF + Lib1 are divided into two bins to describe the corresponding fitting dependences: $t_L < 3$ Gyr (green colour), and $t_L > 3$ Gyr (red colour). For each age bin, we show the median $\chi^2$ with a vertical dashed line, and show the 16th and 84th percentiles with two vertical dotted lines.

In Figs 3 and 4, the lack of metal-rich stars can affect the fitting quality to those high-metallicity spectra, but the selected IMF and isochrones have little effect to the fitting results. Here we compare the fitting results derived from fittings with Lib1 and Lib4 to quantify their relative parameter offsets ($\Delta P = P_{\text{Lib4}} - P_{\text{Lib1}}$).

### 3.3 Empirical stellar spectral library effects

In Figs 3 and 4, the lack of metal-rich stars can affect the fitting quality to those high-metallicity spectra, but the selected IMF and isochrones have little effect to the fitting results. Here we compare the fitting results derived from fittings with Lib1 and Lib4 to quantify their relative parameter offsets ($\Delta P = P_{\text{Lib4}} - P_{\text{Lib1}}$).

Fig. 5 shows the relative parameter offsets caused by Lib1 and Lib4 by applying pPXF and corresponding libraries to MaNGA spectra at S/N = 60. In the six metallicity bins, the biggest difference is shown in the most metal-rich bin. Due to the lack of metal-rich stars in the STELIB library, those supersolar SSP templates are actually constructed based on relatively low-metallicity stars,
which caused an underestimation of the metallicity for those high-metallicity spectra. Based on the current MaNGA galaxy sample, the averaged offsets of the four parameters in the largest metallicity bin ([M/H]_L > 0.1) are shown in violet dashed lines: \( \Delta E(B - V) = 0.03 \pm 0.01 \) mag, \( \Delta \log (M/L_r) = 0.12 \pm 0.07 \) dex, \( \Delta \log (t_L) = 0.19 \pm 0.09 \) dex, and \( \Delta [M/H]_L = -0.15 \pm 0.09 \) dex.

For the solarlike metallicity bin \(-0.2 < [M/H]_L < 0.1\), those spectra with age around 5 Gyr or younger have similar trends as shown in the [M/H]_L > 0.1 bin. For those spectra with \( t_L \sim 10 \) Gyr, the systematic offsets almost disappear. For the left four bins with [M/H]_L < -0.2, there are no clear systematic offsets, and the parameter differences are dominated by scatter.

To explore the dominant reason of those parameter offsets, we first check the relations between these parameter offsets in Fig. 6. For those spectra with [M/H]_L > 0.1, spectral fittings with the Lib4 library can introduce negative offsets of dust extinction relative to that with the Lib1 library. These negative offsets of \( E(B - V) \) correspond to positive offsets of \( M/L_r \) (left-hand panel) and stellar age (middle left panel), and negative offsets of [M/H]_L (middle right panel). In the right-hand panel, we further clarify that the age and metallicity offsets are not caused by the age–metallicity degeneracy. The effect of the age–metallicity degeneracy when performing pPXF fitting at S/N = 60 is shown by the black contours. Most of the data points in the right-hand panel are outside the contours, which means that the parameter offsets \( P_{Lib4} - P_{Lib1} \) are not caused by the age–metallicity degeneracy.

Considering that the S/N of our observed spectra are not uniformly 60, we then plot the dust extinction and metallicity offsets versus the spectral S/N’s in Fig. 7. There is no obvious trend between \( \Delta E(B - V) \) or \( \Delta [M/H]_L \) offsets and S/N, which means that these parameter offsets are also not caused by the S/N effect.

Without the dominant reason from the age–metallicity degeneracy and S/N effects, the parameter offsets of those high-metallicity spectra are most probably caused by the differences between the empirical STELIB and MILES libraries, or code improvement by the Vazdekis model. Since the STELIB library not only lacks the metal-rich stars, but also has other differences compared to MILES, e.g. not corrected from the telluric absorption, we then stack those spectra with \( \chi^2/DOF > 0.2 \) to identify whether these \( \chi^2 \) differences are caused by the continuum or relative chemical abundance. From Fig. 8, we can see that the stacked fitting residuals obtained from the Lib1 (black line) and Lib4 (red line) libraries do not suffer a continuum correction problem. Their main differences happen to those absorption-line features, which indicates that the parameter offsets are most probably caused by differences of the relative chemical abundances. Here we cannot exclude the possibility of code improvement by the Vazdekis model without detailed comparisons of the two models, which is out of the scope of this paper.

With the above reduced \( \chi^2 \) and parameter offsets analyses, we find that the Vazdekis/MILES model can provide better spectral fitting quality than the Galaxev/STELIB model for [M/H]_L > -0.2 cases. Thus, we take the Vazdekis/MILES model for analysing the effects of IMF variation and stellar evolution isochrones.

### 3.4 IMF variation effects

Considering that the empirical MILES library not only has more metal-rich stars, but also covers more complete fundamental parameter space than the STELIB library. We study the IMF variation...
Comparison of different SSP libraries

Figure 6. Relations between different parameter offsets. The $\Delta E(B - V)$ versus $\Delta \log (M_*/L_*)$, $\Delta E(B - V)$ versus $\Delta \log (t_*)$, $\Delta E(B - V)$ versus $\Delta [M/H]_L$, and $\Delta \log (t_*)$ versus $\Delta [M/H]_L$ plots are shown from the left-hand to right-hand panels. In the right-hand panel, we also plot the contours from simulation, which show the effect of age–metallicity degeneracy when performing the pPXF fitting at $S/N = 60$. Each spectrum is plotted as a point coloured by its luminosity-weighted age. The black error bar in each panel shows the median uncertainty of the parameter offsets.

Figure 7. Variations of $\Delta E(B - V)$ (left-hand panel) and $\Delta [M/H]_L$ (right-hand panel) with $S/N$ for the $[M/H]_L > 0.1$ bin. The points are coloured the same as shown in Fig. 6.

Figure 8. The mean fitting residuals of those spectra fitted by the Lib1 (in black colour) and Lib4 (in red colour) libraries. To check whether the fitting differences are caused by the relative chemical abundances, here we only stack those spectra with $\Delta (\chi^2/DOF) > 0.2$, which is the reduced $\chi^2$ difference derived from the Lib1 and Lib4 libraries.
effects by applying Lib1 and Lib2 to the data to obtain the relative parameter offset ($\Delta P = P_{\text{Lib2}} - P_{\text{Lib1}}$), focusing only on the difference between Salpeter and Chabrier IMFs, and keeping the same Padova2000 isochrone and empirical MILES library. In the top panel of Fig. 9, we show the difference in MaNGA spectral fitting results between pPXF + Lib1 and pPXF + Lib2. The parameter offsets caused by IMF variation behave as follows:

(i) The IMF variation causes no significant $E(B-V)$ fitting offset.
(ii) The $\Delta \log (M_*/L_\odot)$ ranging from $-0.2$ to $-0.1$ dex, and the offset values correlate with stellar ages.
(iii) Spectra with old ages (red dashed lines) have larger $\log(t_\text{fit}/\text{yr})$ offsets than those younger ones (green dashed lines).
(iv) The $[\text{M/H}]_\odot$ show increased offsets for those spectra with older ages when $[\text{M/H}]_\odot > -0.5$.

To interpret these relative offsets caused by the Salpeter and Chabrier IMFs, we use simulations to find out the main reason. According to the method shown in Appendix A, we generate mock spectra based on Lib1, then fit these mock spectra using pPXF + Lib1 and pPXF + Lib2, respectively. By analysing the relative parameter offsets calculated from $P_{\text{Lib2}} - P_{\text{Lib1}}$ (bottom panels of Fig. 9), we can check the IMF variation effects and interpret how and why these population parameters are offset. Before comparing with observation, we first summarize the IMF effects in our simulation:

(i) There is no offset for the dust extinction correction in all cases.
(ii) When fitting a spectra with Chabrier IMF, the $M_*/L_\odot$ will be underestimated by $\sim 0.2$ dex at the young ages ($t_\text{fit} = 10^9$ yr). With increased spectral age and poorer metallicity, the $M_*/L_\odot$ differences decrease.
(iii) The age offsets increase from zero for the youngest spectra to a maximum for the oldest spectra. The largest age offsets decrease from metal-poor ($\sim 0.15$ dex) to metal-rich ($\sim 0.1$ dex) bins.
(iv) The metallicity offsets appear, and the values vary from positive offsets at the smallest metallicity to negative offsets at the largest metallicity. These offsets also increase with stellar ages.

These $M_*/L_\odot$, age, and metallicity offsets in the simulation are significant, and the offset trends described above are not affected by the fitting uncertainty, which is reflected by the scatters shown in the bottom panel of Fig. 9. With the simulation results, now we can derive the IMF effects on full-spectrum fitting results, which have been shown partly by the observation. Based on the simulation, we can also identify how the input SFH can be recovered by spectral fitting, and the dominant reason of parameter offsets.

For those spectra with $[\text{M/H}]_\odot > -1.0$, the overestimated stellar ages and underestimated metallicities are mainly caused by two effects: (1) the intrinsic age-metallicity degeneracy, and (2) SSP template difference caused by different IMFs at the same age and metallicity.

Because an SSP template with a younger age and a higher metallicity is similar to the one with an older age and a lower metallicity, the positive offset in stellar age propagates to a negative offset in metallicity.

At young stellar ages, high-mass stars still exist and those low-mass stars contribute very little to the total light. As the SSP ages increase and more high-mass stars explode, the light fraction contributed by low-mass stars will increase. Since the Salpeter IMF contains more low-mass stars than the Chabrier IMF, a given age SSP generated with the Salpeter IMF would have a similar low-mass-star light fraction as that of the Chabrier IMF based SSP with an older age. Therefore, fitting a spectrum with the Chabrier IMF would result in an older age than that with the Salpeter IMF. The resulted parameter offsets increase with stellar ages.

In the right four columns of Fig. 9, the first effect explains why there are $\Delta \log (t_\text{fit})$ and $\Delta [\text{M/H}]_\odot$ offsets, the second effect explains why the age and metallicity offsets increase with older ages.

The recovered SFHs also provide a clear reflection of these two effects. Here we take old spectra ($t_\text{fit} = 10$ Gyr) as examples, as the age and metallicity offsets shown in Fig. 9 increase with stellar ages. In the left-hand panel of Fig. 10, the recovered SFH is dominated by those SSP templates with older ages and lower metallicities.

For the results shown in the left two columns of Fig. 9, the metallicities are measured with positive offsets. This should be mainly due to the limitation of model grid, as there are no SSPs with smaller metallicity for fitting. This can be verified by the middle panel of Fig. 10, which shows an SSP template at the smallest metallicity with the oldest age contributing a high mass fraction.

Since there is no SSP with a smaller metallicity, the fitting finds an SSP with higher metallicity ($[\text{M/H}] = -0.4$) to match the input spectrum.

The age-metallicity degeneracy should be affected by the fundamental parameter coverage of the empirical stellar spectral library. If using a library with fewer stars, the difference in spectral features between those SSP templates with similar ages and metallicities should be more obvious, which means the age-metallicity degeneracy is weak. Therefore, if we use the Galaxev/STELIB-based SSP libraries to check the IMF variation effects, the age-metallicity degeneracy should affect the parameter offsets less than using the Vazdekis/MILES-based SSP libraries.

Fig. 11 shows the comparisons of IMF variation effects ($\Delta P = P_{\text{Lib3}} - P_{\text{Lib1}}$) for both observational spectral (top) and mock spectral (bottom) fitting with the pPXF code. Different IMFs still cause no offset to the dust extinction measurements. For the Galaxev/STELIB model, the $M_*/L_\odot$ derived from the Chabrier IMF are systematically lower by a $\sim 0.2$ dex than that from the Salpeter IMF for both the simulation and observation tests. By comparing Figs 9 and 11, we find that there are smaller age and metallicity offsets when apply the Galaxev/STELIB model based libraries for IMF variation tests.

From the recovered SFH shown in the right-hand panel of Fig. 10, the best spectral fitting catches older SSPs with log($t_\text{fit}/\text{yr}$) = 10.2 rather than log($t_\text{fit}/\text{yr}$) = 10.0 as the peak age, which finally causes a systematic $\sim 0.1$ dex age offset. This is mainly caused by the SSP template difference effect. Considering that the empirical STELIB library only contains $\sim 197$ spectra for calibration, the resolution in the metallicity space may be not sufficiently high. The age-metallicity degeneracy effect is then not obvious in the application of the Galaxev/STELIB model based libraries.

With the understanding of empirical library and IMF effects, we then focus on the comparison of Padova2000 and BaSTI stellar evolution models by using Vazdekis/MILES based SSP libraries.

### 3.5 Effects of stellar evolution isochrones

We select Lib1 and Lib3 libraries to check the relative parameter offsets ($\Delta P = P_{\text{Lib3}} - P_{\text{Lib1}}$) caused by Padova2000 and BaSTI isochrones, with the same setup of empirical MILES library and Salpeter IMF.

In Fig. 12 we plot the relative parameter offsets derived from $P_{\text{Lib3}} - P_{\text{Lib1}}$. These offsets can be summarized as follows:
Comparison of different SSP libraries

Figure 9. Top: The relative parameter offsets ($\Delta P = P_{\text{Lib2}} - P_{\text{Lib1}}$) between the Chabrier and Salpeter IMFs in the case of MaNGA spectral fitting at S/N = 60. In this comparison, Lib1 and Lib2 have the same Vazdekis/MILES model and Padova2000 isochrones. Lines, points, error bars, and colours are the same as described in Fig. 5. In the fifth column, which contains the largest number of data points, we plot the red and green dashed lines to show the median offsets ($\Delta \log (M/L_r)$, $\Delta \log (t_L/a)$, and $\Delta [M/H]_L$) of those old ($t_L > 3 \, \text{Gyr}$) and young ($t_L < 3 \, \text{Gyr}$) spectra, respectively. Bottom: We generate mock spectra based on Lib1, and then perform the fitting with pPXF + Lib1 and pPXF + Lib2. The relative parameter offsets ($P_{\text{Lib2}} - P_{\text{Lib1}}$) in the simulation can be compared with that shown in the top figure. From left to right, we show the six metallicity bins ($[M/H] = -1.71$, $-1.31$, $-0.71$, $-0.4$, $0.0$, $0.22$) bins based on the peak $[M/H]$ of each SFH. Blue to red colours represent the stellar age ranging from 0.063 to 15 Gyr. The offsets in the four parameters ($\Delta (B-V)$, $\Delta \log (M/L_r)$, $\Delta \log (t_L/a)$, and $\Delta [M/H]_L$) are shown from top to bottom. The zero-offset line of each parameter in each panel is labelled as the horizontal dashed line. The error bars indicate the 16th and 84th percentiles.
tend to be positive for those old spectra, but negative for those young.

Figure 12. The only difference is that the results are more scattered
mock spectra are then generated using Lib3. In the bottom panels
metallicities.

means that the current assumption is not reasonable for richer
eters in the simulation are opposite to the observation, which

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by the real spectra as shown in Fig. 12. Otherwise, if the observed
from both simulation (Fig. 13

mock spectra generated using Lib3, then we can conclude that
relative parameter offset trends are similar to that based on the
backwards.

First, we assume that the Padova2000 model is closer to the reality
P = P_{Lib3} − P_{Lib1}) as that yielded
(i) Compared to the fitting with pPXF + Lib1, fittings with pPXF + Lib3 have a maximum ∼0.1 magnitude larger
E(B − V) offsets for those younger spectra (t_{L} < 10^{9.5} yr) in the
metallicity bins −1.5 < [M/H]_{L} < −0.2. Spectra with older ages (t_{L} > 10^{9.5} yr) tend to have smaller E(B − V) offset.
(ii) The measured relative light-weighted ages and M_{L}/L_{o} offsets tend to be positive for those old spectra, but negative for those young spectra.
(iii) The fitted relative [M/H]_{L} offsets increase with younger ages.

For the stellar evolution model analyses, it is hard to predict which
one is closer to the real stellar evolution. However, we can check
which stellar evolution model is closer to the reality by designing
a contrast test. For example, if we assume the Padova2000 model
is closer to the reality, then if we generate mock spectra using
Padova2000 and then fit it with both Lib1 and Lib3, it should yield
similar relative parameter offset (∆P = P_{Lib3} − P_{Lib1}) as that yielded
by the real spectra as shown in Fig. 12. Otherwise, if the observed
relative parameter offset trends are similar to that based on the
mock spectra generated using Lib3, then we can conclude that
the BaSTI model describes the stellar evolution of local galaxies
better.

First, we assume that the Padova2000 model is closer to the reality
than the BaSTI model, and generate the mock spectra based
on Lib1 SSP library. Whether this assumption is correct can be
confirmed by comparing the trends of parameter offsets derived
from both simulation (Fig. 13 top) and observation (Fig. 12).
After the comparison we can see that only the ∆E(B − V) and
∆[M/H]_{L} at low metallicity cases ([M/H]_{L} < −1.0) have similar trends for the simulation and observation tests. When
[M/H]_{L} > −1.0, the parameter offset trends of the four parameters
in the simulation are opposite to the observation, which means
that the current assumption is not reasonable for richer metallicities.

Secondly, we assume the BaSTI model is closer to the reality,
the mock spectra are then generated using Lib3. In the bottom panels
of Fig. 13, the E(B − V) offset trends are the same as shown in
Fig. 12. The only difference is that the results are more scattered in the observation results. For those spectra with [M/H]_{L} > −1.0, the
∆log(M_{L}/L_{o}), ∆log(t_{L}/yr), and ∆[M/H]_{L} show similar offset trends at different ages. For example, in the fifth metallicity bin
(−0.2 < [M/H]_{L} < 0.1) of Fig. 12, the red (t > 3 Gyr) and green (t < 3 Gyr) dashed lines show similar offset trends as shown in

Fig. 13 bottom. However, in low-metallicity bins ([M/H]_{L} < −1.0),
the trends from simulation and observation tests are opposite.

We also explore the relations between parameter offsets and spectral S/N’s at the −0.2 < [M/H]_{L} < 0.1 bin in Fig. 14. From both ∆E(B − V) versus S/N in the left-hand panel and ∆log(t_{L}) versus S/N in the right-hand panel, we can see that at smaller S/N (<60), the parameter offsets are actually contaminated by the S/N. With increasing S/N, the ∆log(t_{L}) differences between the old and young spectra become more clear. At S/N ≥ 60, the offset trends are more likely that shown in the bottom panels of Fig. 13.

Based on the above analyses, we conclude that the Padova2000
model matches the local galaxies better than the BaSTI model at
[M/H]_{L} < −1.0, while the BaSTI model is closer to the local galaxy
evolution than Padova2000 model at [M/H]_{L} > −1.0.

It would be helpful for improving the modelling of stellar evolution isochrones by finding out the detailed differences between the Padova2000 and BaSTI models, and searching for the dominant reason of the above conclusion. However, in this paper, we only present the comparison results and leave the detailed analyses of the two models in future works.

4 DISCUSSION

4.1 Basic assumptions

There are two basic assumptions in this paper: (1) a universal form
of lognormal SFH, and (2) the relative parameter offset is calculated
by assuming that one of the selected five SSP libraries is closer to
real observations.

From Figs 6, 8, 9, and 10 we find that parameter offsets derived
from real spectra are more scattered than the mock ones. This might
be caused by two reasons: (1) our assumed lognormal SFH in the
simulated spectra does not accurately describe the real SFHs in local
realities, (2) none of the five selected SSP libraries can represent
the reality exactly.

As to the relative parameter offsets, our comparison is based on
the fact that there are only small parameter offsets if an SSP library
is closer to the real case. If there are larger difference for both the two
SSP libraries, we cannot derive reasonable values of those relative
parameter offsets based on the simulation.
Comparison of different SSP libraries

4.2 Comparison with previous works

In Gonzales Delgado & Cid Fernandes (2010), they fitted spectra of star clusters and found that the BC03 library can underestimate the metallicity by 0.6 dex. In our work, we find a $\Delta M_*/L_\odot \sim -0.15$ dex offset when we compare the BC03 model to the Vazdekis/MILES model in MaNGA galaxies. Our 0.15 dex relative offset is probably due to the lack of metal-rich stars in the STELIB library compared to the MILES library. The offset obtained in Gonzales Delgado & Cid Fernandes (2010) is the absolute bias, which may be affected by other reasons, such as the model bias and selection of isochrones.

Another thing should be noticed here is that we use the spatially resolved spectra in MaNGA survey, which consist of CSPs. This composition lead to a decrease of the light-weighted [M/H] offsets.

In some previous works (e.g. Bernardi et al. 2010), the $M_*/L$ offset between the Chabrier IMF and Salpeter IMFs is set as 0.25
MNRAS full-spectrum fitting, the variation of each ingredient. By generating mock spectra based on 127-fibers bundle, we derive the parameter offsets caused by the input parameters. The parameter offsets based on those mock spectra with well-known origins of these offsets, we perform simulations and interpret caused by the selected ingredient uncertainty. To further understand ingredients the same, we can easily find out the parameter offsets on only one ingredient variation while keeping the other two SSP libraries to MaNGA galaxies, we can derive the relative comparison at each time. By applying the pPXF code and different the Padova2000 and BaSTI stellar evolutionary isochrones. Chabrier IMFs, the empirical STELIB and MILES libraries, and we focus on two popular options, including the Salpeter and library, and stellar evolution model/isochrones. For each ingredient, used for generating an SSP library: IMF, empirical stellar spectral input parameters.

5 CONCLUSIONS

In this paper, we study model uncertainties of the three ingredients used for generating an SSP library: IMF, empirical stellar spectral library, and stellar evolution model/isochrones. For each ingredient, we focus on two popular options, including the Salpeter and Chabrier IMFs, the empirical STELIB and MILES libraries, and the Padova2000 and BaSTI stellar evolutionary isochrones.

In total, we select five SSP libraries, and take two libraries for comparison at each time. By applying the pPXF code and different SSP libraries to MaNGA galaxies, we can derive the relative parameter offsets caused by different libraries. When focusing on only one ingredient variation while keeping the other two ingredients the same, we can easily find out the parameter offsets caused by the selected ingredient uncertainty. To further understand the origins of these offsets, we perform simulations and interpret the parameter offsets based on those mock spectra with well-known input parameters.

By using 100 randomly selected MaNGA galaxies observed with 127-fibers bundle, we derive the parameter offsets caused by the variation of each ingredient. By generating mock spectra based on assumed lognormal SFH and MEH, we perform the same fitting and investigate the dominate reason of the offsets.

The SSP libraries based on the Vazdekis/MILES model introduce significant improvements on the reduced $\chi^2$ distributions than those based on the Galaxev/STELIB model, which might means a better fundamental space coverage can match the observed spectra better. From our comparison, the $\chi^2$ improvement mainly happens to the metal-rich case with $[\text{M/H}]_L > -0.2$. Based on our detailed analyses, the parameter offsets at the oversolar metallicity bin are caused by differences of the relative chemical abundances or stellar population synthesis code improvements, instead of the age–metallicity degeneracy or S/N effects. In the $[\text{M/H}]_L$ fundamental space coverage can match the observed spectra better. However, significant differences appear when comparing the metal-rich case with $[\text{M/H}]_L > -0.2$. Based on our detailed analyses, the parameter offsets at the oversolar metallicity bin are caused by differences of the relative chemical abundances or stellar population synthesis code improvements, instead of the age–metallicity degeneracy or S/N effects. In the $[\text{M/H}]_L$ bin, the Galaxev/STELIB based model can introduce $\sim 0.15$ dex lower $[\text{M/H}]_L$, $\sim 0.19$ dex older stellar ages, and $\sim 0.12$ dex larger log ($M_*/L_\text{r}$) than those with Vazdekis/MILES based libraries. The $M_*/L_\text{r}$ derived from the Chabrier IMF are of course systematically lower than that from the Salpeter IMF by a median of $\sim 0.22$ dex from the Galaxev/STELIB model, but $\sim 0.15$ dex from the Vazdekis/MILES model. When one fit a spectrum with different IMFs, the parameter offsets not only appear to $M_*/L_\text{r}$, but also age and metallicity. If we apply the Vazdekis/MILES based libraries for spectral fitting, the offsets in fitted stellar ages and metallicities increase with the age of the populations. However, when applying the Galaxev/STELIB model based libraries for test, due to their less complete fundamental parameter coverage than the MILES library, the relative parameter offsets have no metallicity dependence.

With the MaNGA spectra, the variation of stellar evolutionary isochrones introduces no improvements in the reduced $\chi^2$ distributions. However, significant differences appear when comparing parameters derived with the two isochrones. To check the origin of
Comparison of different SSP libraries

Figure 13. **Top**: The mock spectra are generated based on the Lib1 library, then spectral fittings are performed with pPXF + Lib1 and pPXF + Lib3. The relative parameter offsets ($P_{\text{Lib3}} - P_{\text{Lib1}}$) in the simulation can be compared with that shown in Fig. 12. **Bottom**: The mock spectra are generated based on Lib3 library, then the spectral fitting and analyses of relative parameter offsets are performed in the same way as done in the Top figure. Lines, points, and colours are the same as described in Fig. 9.

For the spectral fitting of local galaxies, we would suggest to select the empirical MILES library to avoid the measurement offsets against rich metallicities, and the BaSTI isochrone due to its closer match to the local galaxy evolution. If a galaxy has potential radial IMF variation, spectral fitting with a fixed IMF as a function of the Padova2000 one. With increasing spectral S/N’s, the evidence becomes more robust.
of radius will introduce age-dependent offsets of $M_r/L$, age, and metallicity when the Vazdekis/MILES model based SSP libraries are applied.

Finally, we emphasize that it will be important to expand high-resolution stellar libraries, such as the ongoing MaNGA Stellar Library (MaStar; Yan et al. 2018).

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Figure 14. Variations of $\Delta(E(B-V))$ (left-hand panel) and $\Delta\log(t_L)$ (right-hand panel) with S/N for the $-0.2 < [M/H] < 0.1$ bin. The points are coloured by the luminosity-weighted stellar ages as shown in the right colourbar. The red and green lines shown in each panel are defined the same as shown in Fig. 12.
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APPENDIX A: SIMULATIONS

When applying the observed spectra for model uncertainty analyses, one potential problem is: even when we divide the spectral sample into detailed subsamples, it is hard to have a thorough understanding of the origin of these offsets. We interpret these model uncertainties further using mock data. To match the observed spectra, we need to construct the galaxy star formation history (SFH) and metallicity enrichment history (MEH).

A1 Construction of SFH and MEH

Many efforts have been dedicated to the study of SFH of different kinds of galaxies, the lognormal SFH tends to be a simple model and have been supported by many observations (e.g. Gladders et al. 2013; Pacifici et al. 2016). We then assume a lognormal SFH and metal enrichment history (MEH) as follows:

\[
\text{SFH}(M_\odot, \text{yr}^{-1}) = \frac{1}{\sqrt{2\pi\tau}} \exp\left(\frac{(t - t_0)^2}{2\tau^2}\right). \tag{A1}
\]

\[
\text{MEH}(Z) = \frac{1}{\sqrt{2\pi\tau}} \exp\left(\frac{(Z - Z_0)^2}{2\tau^2}\right). \tag{A2}
\]

Based on our constructed SFH and MEH, Fig. A1 shows the SFH in the age space (top panel) and metallicity space (bottom panel)
Figure A1. Lognormal SFH (top panel) and (MEH) (bottom panel) adopted for generating mock spectra. The top panel shows 25 SFH curves adopted to generate mock spectra, with the peak SSP age shown by the right colour bar (blue to red: young to old). The bottom panel shows 6 MEHs by setting each SSP peak metallicity from poor to rich, where metallicities are labelled with purple to yellow colours.

by setting the colour of each curve according to the peak of the lognormal distribution.

The final SFH–MEH map in the age–metallicity parameter space can be obtained, which appears the same as the fitted results. Here we show three examples with different age and metallicity peaks in Fig. A2.

We then use the assumed SFH-MEH map to generate mock spectra, which are then used for model offset analyses.

A2 Mock data generation and spectral fitting

With the constructed SFH, we first obtain the mass fraction of each SSP, then convert the corresponding mass fraction of each SSP to light fraction based on $M_*/L_r$. A mock spectrum is then generated based on the r-band light fraction of each SSP. According to the different wavelength coverages of Galaxev/STELIB and Vazdekis/MILES models, we set the spectral fitting range of mock data to 3600–7350 Å, which eliminates ∼50 Å at both the blue and red end to make sure the model SSPs have larger spectral coverage than mock spectra.

Due to the different spectral resolutions of Galaxev/STELIB (FWHM = 2.76 Å) and Vazdekis/MILES (FWHM = 2.54 Å), all the mock spectra generated based on Vazdekis/MILES libraries are smoothed to FWHM = 2.76 Å. The MaNGA spectral resolution is similar to Galaxev/STELIB library, with a velocity scale of 69 km s$^{-1}$ (Albareti et al. 2017). The mock spectra are then sampled in logarithmic wavelength grid, which is required by pPXF, and the velocity scale is uniformly set to 69 km s$^{-1}$. To make our mock spectra more like observed ones, we artificially add a 100 km s$^{-1}$ velocity dispersion added mock spectra. The final generated mock spectra have S/N = 60 at 5500 Å (median S/N at the wavelength window [5490, 5510] Å).

During spectral fitting, we use the full spectral information with emission-line regions masked, to match the fitting done to the MaNGA data. The current version of pPXF can fit both the stellar emission and gas emission together. In Ge et al. (2018), we avoid the emission line fitting since STARLIGHT code can only fit the stellar spectra, here we also turn-off the emission line fitting process and only focus on stellar continuum fitting.

For dust extinction curves in different galaxies, we allow the input $E(B-V)$ to vary from 0.0 to 0.5 as done in Ge et al. (2018), by adopting the CAL (Calzetti et al. 2000) dust reddening curve.

A3 Parameter biases of the pPXF fitting at S/N = 60

In Ge et al. (2018), we have checked the pPXF fitting biases at S/N = 60 for those single-SSP or two-components SSPs based mock spectra. With the assumed SFH here, we do the same tests to check the parameter biases if performing the pPXF fitting at S/N = 60.

Fig. A3 shows the fitted parameter biases based on the pPXF and Lib1 SSP library. At S/N = 60, using pPXF we can constrain the dust extinction within 0.01 magnitude. For the recovered log $(t_L)$ and $[M/H]_r$, all the biases and scatters in different ages have their median values less than 0.1 dex. The same thing happens to $M_*/L_r$, except for those spectra with stellar ages less than 0.3 Gyr, which have larger scatters and are rare in local galaxies.

Kacharov et al. (2018) tested the pPXF fitting to spectra of the nuclear star clusters in six nearby galaxies. They found that even...
Comparison of different SSP libraries

Figure A2. Three mock SFH examples with the peak age and metallicity located at \([\log(t/\text{yr}), [\text{M/H}]] = [8.0, -1.71], [9.0, -0.4], \text{ and } [10.0, 0.22]\). In each panel, the right colour bar indicates the linear mass fraction of each SSP components.

Figure A3. The fitted parameter biases of the pPXF fitting with Lib1 SSP library at S/N = 60 in different metallicity bins. We generate mock spectra based on Lib1, and then perform the fitting with pPXF + Lib1. The relative parameter bias \((P_{\text{fit}} - P_{\text{input}})\) reflects the effects of age–metallicity degeneracy and spectral S/N. From left to right, we show the six metallicity bins \([\text{M/H}] = -1.71, -1.31, -0.71, -0.4, 0.0, 0.22\) bins based on the peak \([\text{M/H}]\) of each SFH. Blue to red colours represent the stellar age ranging from 0.063 to 15 Gyr. The biases in the four parameters \((\Delta E(B-V), \Delta \log (M_*/L_r), \Delta \log t_L, \text{ and } \Delta [\text{M/H}]_L)\) are shown from top to bottom. The zero-bias line of each parameter in each panel is labelled as the horizontal dashed line. The error bars indicate the 16th and 84th percentiles.

in more complex SFH cases (see their Figs 5–13), the pPXF code could still provide a good recovery of the input SFH.

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