Optimal Resource Allocation for Cellular Networks with Virtual Cell Joint Decoding

Michal Yemini  
Wireless Systems Laboratory  
Stanford University  
California, USA  
michalye@stanford.edu

Andrea J. Goldsmith  
Wireless Systems Laboratory  
Stanford University  
California, USA  
andrea@wsl.stanford.edu

Abstract—This work presents a new resource allocation optimization framework for cellular networks using neighborhood-based optimization. Under this optimization framework resources are allocated within virtual cells encompassing several base-stations and the users within their coverage area. Incorporating the virtual cell concept enables the utilization of more sophisticated cooperative communication schemes such as coordinated multi-point decoding. We form the virtual cells using hierarchical clustering given a particular number of such cells. Once the virtual cells are formed, we consider a cooperative decoding scheme in which the base-stations in each virtual cell jointly decode the signals that they receive. We propose an iterative solution for the resource allocation problem resulting from the cooperative decoding within each virtual cell. Numerical results for the average system sum rate of our network design under hierarchical clustering are presented. These results indicate that virtual cells with neighborhood-based optimization leads to significant gains in sum rate over optimization within each cell, yet may also have a significant sum-rate penalty compared to fully-centralized optimization.

I. INTRODUCTION

The increased capacity demand in cellular networks is a major driver in the deployment of 5G systems. To increase network capacity, the deployment of small cells has been proposed and is currently taking place [1]–[4]. The main caveat of the usage of small cells is that their proximity to one another combined with their frequency reuse can cause severe interference which must be managed carefully to maximize the overall network capacity. To reduce interference a new interference mitigation paradigm called Cooperative Multi-Point (CoMP) was proposed (see [5]). This paradigm encompasses several cooperation models such as Uplink Interference Prediction in which cooperation is allowed in the resource allocation stage only, and the Uplink Joint Detection model that we consider in this work which allows base-station cooperation in both the resource allocation and decoding stages. We investigate a flexible cooperative resource allocation structure for cellular systems where, instead of each base-station serving all users within its own cell independently, several base-stations act cooperatively to create a “virtual cell” in which the base-stations jointly decode their signals. To design wireless networks that are composed of virtual cells we address in this work the following two design challenges: 1) Creating the virtual cells, i.e., clustering the base-stations into virtual cells. 2) Allocating the resources in each virtual cell assuming cooperative decoding with infinite-capacity backhaul links between base-stations in each virtual cell.

Base-station and user clustering as part of network performance enhancement is discussed in the CoMP literature, see for example [6]–[17]. The clustering of base-stations and users can be divided into three groups: 1) Static clustering which considers a cellular network whose cells are clustered statically. Hence, the clustering does not adapt to network changes. Examples for static clustering algorithms are presented in [7]–[10]. 2) Semi-dynamic clustering, in which static clusters are formed but the cluster affiliation of users is adapted according to the networks changes. Examples for such algorithms are presented in [11]–[13]. 3) Dynamic clustering in which the clustering of both base-stations and users adapts to changes in the network. Examples for dynamic clustering algorithms are presented in [14]–[16]. For an extensive literature survey of cell clustering for CoMP in wireless networks see the work [6]. Finally, cell clustering strategies in wireless networks is also investigated in the ultra-dense network literature, see for example [18]–[23].

Resource allocation for virtual cell joint decoding is closely related to cloud radio access network [24]–[28] in which several cells act cooperatively. Interestingly, maximizing the user sum rate in a virtual cell is equivalent to maximizing the sum rate of a multiple access channel with multiple receiving antennas and several frequency bands. Thus, the optimal resource allocation scheme in a virtual cell in terms of user sum rate is capacity-achieving. Furthermore, this optimal resource allocation can be calculated by convex optimization techniques.

II. PROBLEM FORMULATION

We consider a communication network that comprises a set of base-stations (BSs) $\mathcal{B}$, a set of users $\mathcal{U}$ and a set of frequency bands $\mathcal{K}$. The users communicate with the BSs which can choose to cooperatively decode their signals. Each user $u \in \mathcal{U}$ has a power constraint of $P_u$ dBm. To form the neighborhood in which decoding is performed cooperatively the BSs and
users are clustered into virtual cells which must fulfill the following characteristics.

A. Virtual Cells

Definition 1 (Virtual BS): Let \( b_1, \ldots, b_n \) be \( n \) BSs in a communication network, we call the set \( \{b_1, \ldots, b_n\} \) a virtual BS.

Definition 2 (Proper clustering): Let \( B \) be a set of BSs, \( U \) be a set of users. Denote \( V = \{1, \ldots, V\} \). For every \( v \), define the sets \( \mathcal{B}_v \subset B \) and \( \mathcal{U}_v \subset U \). We say that the set \( V \) is a proper clustering of the sets \( B \) and \( U \) if \( B_v \) and \( \mathcal{U}_v \) are partitions of the sets \( B \) and \( U \), respectively. That is, \( \bigcup_{v \in V} B_v = B \) and \( \bigcup_{v \in V} \mathcal{U}_v = U \). Additionally, \( B_{v_1} \cap B_{v_2} = \emptyset \) and \( \mathcal{U}_{v_1} \cap \mathcal{U}_{v_2} = \emptyset \) for all \( v_1, v_2 \in V \) such that \( v_1 \neq v_2 \).

Definition 3 (Virtual cell): Let \( B \) be a set of BSs, \( U \) be a set of users, and \( V \) be a proper clustering of \( B \) and \( U \). For every \( v \in V \) the virtual cell \( C_v \) is composed of the virtual BS \( B_v \) and the set of users \( \mathcal{U}_v \).

This condition ensures that every BS and every user belongs to exactly one virtual cell.

Let \( V \) be a proper clustering of the set of BSs \( B \) and the set of users \( U \), and let \( \{C_v\}_{v \in V} \) be the set of virtual cells that \( V \) creates. In each virtual cell \( C_v \) we assume that the BSs that compose the virtual BS \( B_v \) allocate their resources jointly.

B. The Uplink Resource Allocation Problem for CoMP Decoding

In each virtual cell we consider uplink cloud decoding with infinite capacity. For a single frequency band scenario, this setup is equivalent to a multiple access channel with multiple users, each with a single transmitting antenna, and multiple receiving antennas. Denote by \( x_{u,k} \) the signal of user \( u \) in frequency band \( k \), and by \( y_{b,k} \) the received signal at BS \( b \) in frequency band \( k \) in \( K \). For the sake of clarity, we label the BSs in the cluster \( v \) by \( b_1, \ldots, b_{|B_v|} \), and label the users in cluster \( v \) by \( u_1, \ldots, u_{|U_v|} \). Denote \( y_{v,k} \equiv \left( y_{b_1,k}, \ldots, y_{b_{|B_v|},k} \right)^T \) and let \( x_{v,k} \equiv \left( x_{u_1,k}, \ldots, x_{u_{|U_v|},k} \right)^T \), where \((\cdot)^T \) denotes the transpose operator. The receiving signal at BS \( b \in B_v \), ignoring the interference from other virtual cells, in frequency band \( k \) is \( y_{b,k} = \sum_{i=1}^{|B_v|} h_{u_i,b,k} x_{u_i,k} + n_{b,k} \), where \( h_{u_i,b,k} \) is the channel coefficient from user \( u_i \) in \( v \) to the BS \( b \) in \( k \) over frequency band \( k \), and \( n_{b,k} \) is a white Gaussian noise at BS \( b \) over frequency band \( k \).

Let \( h_{u_i,b,k} = (h_{u_i,b_1,k}, \ldots, h_{u_i,b_{|B_v|},k})^T \) be the channel coefficient vector between user \( u_i \) in \( v \) to all the BSs in cluster \( v \), then receiving signal vectors at the BSs in \( v \) is \( y_{v,k} = \sum_{i=1}^{|U_v|} h_{u_i,b,k} x_{u_i,k} + n_{v,k} \), where \( n_{v,k} = (n_{b_1,k}, \ldots, n_{b_{|B_v|},k}) \) is a white noise vector at the BSs. Denote \( C_{v,k} = \text{cov}(x_{v,k}) \) and \( N_{v,k} = \text{cov}(n_{v,k}) \) and let \( \mathcal{W} \) be the bandwidth of frequency band \( k \); the sum capacity of the uplink, ignoring interference outside the virtual cell, in the virtual cell is then:

\[
\max_{k \in K} \sum_{k \in K} W_k \log_2 \left| I + \sum_{u \in U_v} p_{u,k} h_{u,k} h_{u,k}^\dagger N_{v,k}^{-1} \right|
\]

s.t.
\[
\sum_{k \in K} p_{u,k} \leq \mathcal{P}_u, \quad p_{u,k} \geq 0 \quad \forall k \in K,
\]

where \( h_{u,k}^\dagger \) is the conjugate transpose of \( h_{u,k} \) and \( |A| \) denotes the determinant of the matrix \( A \). We assume that the matrix \( N_{v,k} \) is invertible for all \( k \) and thus also positive definite.

We note that the problem (1) ignores interference that is caused by transmissions outside the virtual cell, instead it only considers interference that is caused by transmissions in the virtual cell. However, as the number of virtual cells decreases, this interference becomes the dominant one. Indeed, numerical results show that incorporating virtual cells improves performance monotonically as the number of virtual cells in the network decreases.

III. FORMING THE VIRTUAL CELLS

This section presents the clustering approaches that create the virtual cells within which the resource allocation scheme we present in Section IV operates. We consider two methods to cluster the BSs. The first is a hierarchical clustering of the BS according to a minimax linkage criteria. To evaluate the performance of this clustering method we compare it to an exhaustive search over all the possible clusterings of BSs.

A. Base-Station Clustering

1. Hierarchical clustering - Minimax linkage [29]: Let \( d : \mathbb{R}^2 \times \mathbb{R}^2 \rightarrow \mathbb{R} \) be the Euclidean distance function.

Definition 4 (Radius of a set around point): Let \( S \) be a set of points in \( \mathbb{R}^2 \), the radius of \( S \) around \( s_i \) in \( S \) is defined as \( r(s_i, S) = \max_{s_j \in S} d(s_i, s_j) \).

Definition 5 (Minimax radius): Let \( S \) be a set of points in \( \mathbb{R}^2 \), the minimax radius of \( S \) is defined as \( r(S) = \min_{s_i \in S} r(s_i, S) \).

Algorithm 1 presents the hierarchical clustering algorithm using the minimax linkage criterion; it gets a set of points \( S \) and produces the clusterings \( B_1, \ldots, B_n \), where \( B_m \) is the clustering of size \( m \). Let \( S = \{s_1, \ldots, s_n\} \) be the set of locations of the BSs in \( B \). We use Algorithm 1 with the input \( S \) to create the virtual BSs for each number of clusters \( m \).

Algorithm 1

1. Input: \( S = \{s_1, \ldots, s_n\} \);
2. Set \( B_n = \{\{s_1\}, \ldots, \{s_n\}\} \);
3. Set \( d(\{s_1\}, \{s_j\}) = d(s_1, s_j), \forall s_i, s_j \in S \);
4. for \( m = n - 1, \ldots, 1 \) do
5. Find \( (S_1, S_2) = \arg\min_{G \in B_n, G \neq H} d(G, H) \);
6. Update \( B_m = B_{m+1} \setminus \{S_1 \cup S_2\} \setminus \{S_1, S_2\} \);
7. Calculate \( d(S_1 \cup S_2, G) \) for all \( G \in B_m \);
8. end for

The hierarchical clustering is important to our setup since it enjoys a key property that both the K-means clustering and the spectral clustering lack, namely, the number of clusters can be changed without disassembling all the clusters in the networks. Thus, the number of virtual BSs can be easily adapted.
according to the current state of the network. Moreover, at each stage of Algorithm [1] the minimax linkage criterion minimizes the radius of the new cluster that is created by the merging of two existing clusters. Since interference increases on average as distance decreases this criterion merges two clusters to create a new one in which the minimal interference is maximized on average; this interference is then optimized in the resource allocation scheme. Finally, the minimax linkage criterion enjoys several desirable properties that are discussed in [29].

b) Exhaustive Search: To evaluate the performance of hierarchical clustering against a theoretical upper bound we also performed exhaustive search over all the possible clusterings of BSs. In this way, for a given number of clusters (virtual BSs) we produced all the possible clusterings of BSs and in the end, after calculating the power allocation of all the virtual cells, chose the clustering that yielded the maximal sum rate of the network. This maximal sum rate considered interference from other virtual cells, given the number of clusters and the user affiliation rule.

B. Users’ Affiliation with Clusters

To create the virtual cells, we consider two affiliation rules: 1) Closest BS rule in which each user is affiliated with its closest BS. 2) Best channel rule in which each user is affiliated with the BS to which it has the best channel (absolute value of the channel coefficient). Then each user is associated with the virtual BS that its affiliated BS is part of. This way every virtual BS and it associated users compose a virtual cell.

It is easy to verify that these formations of the virtual cells fulfill the requirement presented in Section II-A.

IV. RESOURCE ALLOCATION FOR JOINT DECODING

This section is dedicated to solving the problem [1] that is presented in Section II-B in which BSs use cloud decoding with backhaul links of infinite capacity.

Using the identity $|AB| = |A| \cdot |B|$ we have that the capacity of the virtual cell is

$$\max_{u,k} \sum_{u,k} W_k \left[ \log_2 \left( N_{v,k} + \sum_{u \in \mathcal{U}_u} p_{u,k} h_{u,k} \| h_{u,k} \| \right) - \log_2 |N_{v,k}| \right]$$

s.t.: $\sum_{u,k} p_{u,k} \leq P_{u,k}$, $p_{u,k} \geq 0$. \hspace{1cm} (2)

Since the terms $\log_2 |N_{v,k}|$ are constants, hereafter we omit them from the objective function. Denote $p_u = (p_{u_1}, \ldots, p_{u,K})$ and let:

$$f (p_{u_1}, \ldots, p_{u_{|\mathcal{U}_u|}}) = \log_2 \left( N_{v,k} + \sum_{u \in \mathcal{U}_u} p_{u,k} h_{u,k} \| h_{u,k} \| \right).$$

The following three conditions must hold in order to optimally solve the problem (2) iteratively using the cyclic coordinate ascend algorithm [30, Chapter 2.7]:

1) The function $f (p_{u_1}, \ldots, p_{u_{|\mathcal{U}_u|}})$ is concave.

2) Define

$$\mathcal{P} \triangleq \left\{ \left( p_{u_1}, \ldots, p_{u_{|\mathcal{U}_u|}} \right) : \sum_{k \in \mathcal{K}} p_{u,k} \leq P_u, \sum_{k \in \mathcal{K}} p_{u,k} \geq 0 \quad \forall \ u \in \mathcal{U}_u \right\},$$

$$\mathcal{P}_u \triangleq \left\{ p_u : \sum_{k \in \mathcal{K}} p_{u,k} \leq P_u, \ p_{u,k} \geq 0 \right\},$$

then $\mathcal{P} = \mathcal{P}_{u_1} \times \ldots \times \mathcal{P}_{u_{|\mathcal{U}_u|}}$. \hspace{1cm} (3)

3) The problem

$$\max f (p_{u_1}, \ldots, p_{u_{|\mathcal{U}_u|}}, \tilde{p}_{u_1}, p_{u_{i+1}}, p_{u_{|\mathcal{U}_u|}})$$

s.t.: $\tilde{p}_{u_i} \in \mathcal{P}_{u_i}$, \hspace{1cm} (4)

has a unique maximizing solution.

Next we solve the problem (4) and show the optimal solution is uniquely attained. Denote $\Sigma_{i,k} = N_{v,k} + \sum_{j \neq i} p_{u_j,k} h_{u_j,k} h_{u_j,k}^\dagger$. The problem (4) is then

$$\max \sum_{k \in \mathcal{K}} W_k \log_2 \left| \Sigma_{i,k} + p_{u_i,k} h_{u_i,k} h_{u_i,k}^\dagger \right|$$

s.t.: $\sum_{k \in \mathcal{K}} p_{u_i,k} \leq P_{u_i}$, $p_{u_i,k} \geq 0 \ \forall k \in \mathcal{K}$. \hspace{1cm} (5)

The Karush–Kuhn–Tucker (KKT) conditions for (5) are

$$W_k \frac{h_{u_i,k} \Sigma_{i,k}^{-1} h_{u_i,k}}{1 + h_{u_i,k} \Sigma_{i,k}^{-1} h_{u_i,k} p_{u_i,k}} - \lambda + \mu_k = 0,$$

$$\lambda \left( \sum_{k \in \mathcal{K}} p_{u_i,k} - P_{u_i} \right) = 0, \ \mu_k p_{u_i,k} = 0,$$

$$\sum_{k \in \mathcal{K}} p_{u_i,k} \leq P_{u_i}, \ \ p_{u_i,k} \geq 0,$$

$$\mu_k \geq 0, \ \lambda \geq 0 \ \forall k \in \mathcal{K}.$$ \hspace{1cm} (6)

Since $\mu_k$ is nonnegative for all $k$, and the matrix $\Sigma_{i,k}^{-1}$ is positive definite for all $k$, in order to fulfill the first KKT condition $\lambda$ must be strictly positive. Now, if $p_{u_i,k} > 0$ then $\mu_k = 0$ and by the first KKT condition

$$p_{u_i,k} = \frac{W_k}{\lambda} - \frac{1}{h_{u_i,k} \Sigma_{i,k}^{-1} h_{u_i,k}}.$$

Also, if $p_{u_i,k} = 0$, then by the first KKT condition

$$W_k h_{u_i,k} \Sigma_{i,k}^{-1} h_{u_i,k} + \mu_k = \lambda.$$ It follows that

$$p_{u_i,k} = \left( \frac{W_k}{\lambda} - \frac{1}{h_{u_i,k} \Sigma_{i,k}^{-1} h_{u_i,k}} \right)^+$$

where $\lambda$ is chosen such that $\sum_{k \in \mathcal{K}} p_{u_i,k} = P_{u_i}$.

\[\text{Since } N_{v,k} \text{ is a positive definite matrix, } \Sigma_{i,k}^{-1} \text{ is positive definite as well.}\]
loss model of Normal shadowing with standard deviation of in each frequency band we consider Rayleigh fading, Log-

20 KHz, the carrier frequency was set to 1800

increases. Second, it shows that for a sufficiently large number

as the number of virtual cells decreases, the average sum rate

insights and conclusions. First, it confirms the expectation that

and spectral clustering. Fig. 1 leads to several interesting

methods presented in [32] algorithms, where the spectral clustering was performed for two possible values of \( \sigma: \sqrt{2000} \) and 2000. Both of these values yielded similar network performance.

We also compared the average system sum rate achieved by joint decoding to the one achieved by single user decoding. The resource allocation problem for single user decoding is nonconvex, so there are multiple methods to approximately solve it, as detailed in [33]. Fig. 2 compares the average system sum rate achieved by joint decoding against the maximal average system sum rate achieved by the single user decoding methods presented in [33], for each number of virtual cells. The virtual cells were generated by using the hierarchical clustering presented in Algorithm 1. We simulated a network with a larger number of users and BSs, specifically 100 users and 20 BSs. The simulation results are shown in Fig. 2, in which we compare the joint and single user decoding for both the closest BS and best channel user affiliation rules. Fig. 2 demonstrates the performance improvement that incorporating virtual cells in the network provides, including the significant sum rate gain of fully centralized versus fully distributed optimization with joint decoding. It also shows that joint decoding can achieve significantly higher average system sum rate compared with single user decoding. However, single user decoding may yield higher sum rate in fully distributed setups in which ignoring out of cell interference affects the joint decoding scheme more severely since it depends on the covariance matrix of the interference and not just its diagonal.

V. NUMERICAL RESULTS

This section presents Monte Carlo simulation results that compare the resource allocation and user affiliation schemes for both the hierarchical clustering and the exhaustive search over all possible clustering. We set the following parameters for the simulation: the network is comprised of 6 BSs and 50 users which were uniformly located in a square of side 2000 meters. There were 10 frequency bands each of bandwidth 20 KHz, the carrier frequency was set to 1800 MHz. The noise power received by each BS was \(-174 \text{ dBm/Hz}, \) and the maximal power constraint for each user was 23 dBm. Finally, in each frequency band we consider Rayleigh fading, Log-Normal shadowing with standard deviation of 8 dB and a path loss model of \( PL(d) = 35 \log_{10}(d) + 34 \) where \( d \) denotes the distance between the transmitter and the receiver in meters (see [51]). We averaged the results over 500 realizations, in each we generated randomly the locations of the BSs, users and channel coefficients. In the simulation we compared the average sum rate achieved by each of the clustering and user affiliation schemes presented in this paper for cooperative decoding. We note that while the resource allocation ignored the interference caused by other virtual cells, the sum rate of the network was calculated considering this interference in the SINR of each user and the corresponding sum rate of that user.

Fig. 1 compares the average system sum rate as a function of the number of virtual cells for the resource allocation scheme presented in Section IV We compared the performance of the two BS clustering methods presented in III-A with those of other BS clustering methods, namely K-means and spectral clustering. Fig. 1 leads to several interesting insights and conclusions. First, it confirms the expectation that as the number of virtual cells decreases, the average sum rate increases. Second, it shows that for a sufficiently large number of frequency bands, the closest BS user affiliation rule and the best channel affiliation rule lead to similar performance. Third, it compares the performance of the hierarchical clustering and the exhaustive search over all BS clustering. This comparison illustrates that, while the exhaustive search outperforms the hierarchical clustering as expected, hierarchical clustering has similar performance with a much lower complexity. Additionally, Fig. 1 shows that clustering BSs using the hierarchical approach with the minmax linkage criterion outperforms clustering the BSs using either K-means or spectral clustering [32] algorithms, where the spectral clustering was performed for two possible values of \( \sigma: \sqrt{2000} \) and 2000. Both of these values yielded similar network performance.

VI. CONCLUSION AND FUTURE WORK

This work addresses the role of virtual cells in resource allocation for future CoMP cellular networks. It addresses two design aspects of this optimization; namely, forming the virtual cells and allocating the communication resources in each virtual cell assuming cooperative decoding. We propose the use of hierarchical clustering in forming the virtual cells so that changing the number of virtual cells only causes local changes and does not force a recalculation of all the virtual base-stations in the network. We also solved the uplink resource allocation problem optimally for cooperative decoding in each virtual cell. Finally, we present numerical results for these methods and discuss the merits of using virtual cells. We note that other hierarchical clustering algorithms can be considered in order to improve the overall network performance. Additionally, other models of cooperation in virtual cells can be considered as well.
Fig. 2. Comparison between the average sum rate of joint and single user decoding as a function of the number of virtual cells using hierarchical BS clustering with minimax linkage criterion.

REFERENCES

[1] V. Chandrasekhar, J. G. Andrews, and A. Gatherer, “Femtocell networks: a survey,” IEEE Communications Magazine, vol. 46, no. 9, pp. 59–67, Sept 2008.
[2] H. Claussen, L. T. W. Ho, and L. G. Samuel, “An overview of the femtocell concept,” Bell Labs Technical Journal, vol. 13, no. 1, pp. 221–245, Spring 2008.
[3] J. G. Andrews, H. Claussen, M. Dohler, S. Rangan, and M. C. Reed, “Femtocells: Past, present, and future,” IEEE Journal on Selected Areas in Communications, vol. 30, no. 3, pp. 497–508, April 2012.
[4] M. B. A. Anpalagan and R. Vannithamby, Design and Deployment of Small Cell Networks. Cambridge University Press, 2015.
[5] R. Irmer, H. Droste, P. Marsch, M. Grieber, G. Fettweis, S. Brueck, H. Mayer, L. Thiele, and V. Jungnickel, “Coordinated multipoint: Concepts, performance, and field trial results,” IEEE Communications Magazine, vol. 49, no. 2, pp. 102–111, February 2011.
[6] S. Bassoy, H. Farooq, M. A. Imran, and A. Imran, “Coordinated multipoint clustering schemes: A survey,” IEEE Communications Surveys Tutorials, vol. 19, no. 2, pp. 743–764, Secondquarter 2017.
[7] S. S. Ali and N. Saxena, “A novel static clustering approach for CoMP,” in 2012 7th International Conference on Computing and Convergence Technology (ICCCT), Dec 2012, pp. 757–762.
[8] H. Shimodaira, G. K. Tran, K. Araki, K. Sakaguchi, S. Konishi, and S. Namba, “Diamond cellular network — optimal combination of small power basestations and CoMP cellular networks;” in 2013 IEEE 24th International Symposium on Personal, Indoor and Mobile Radio Communications (PIMRC Workshops), Sept 2013, pp. 163–167.
[9] A. Barbieri, P. Gaal, S. Geirhofer, T. Ji, D. Malladi, Y. Wei, and F. Xue, “Coordinated downlink multi-point communications in heterogeneous cellular networks,” in 2012 Information Theory and Applications Workshop, Feb 2012, pp. 7–16.
[10] A. M. Hamza and J. W. Mark, “A clustering scheme based on timing requirements in coordinated base-stations cooperative communications,” in 2013 IEEE Wireless Communications and Networking Conference (WCNC), Apr 2013, pp. 3764–3769.
[11] F. Huang, Y. Wang, J. Geng, M. Wu, and D. Yang, “Clustering approach in coordinated multi-point transmission/reception system,” in 2010 IEEE 72nd Vehicular Technology Conference - Fall, Sept 2010, pp. 1–5.
[12] S. A. Ramprashad, G. Caire, and H. C. Papadopoulos, “A joint scheduling and cell clustering scheme for mu-mimo downlink with limited coordination,” in 2010 IEEE International Conference on Communications, May 2010, pp. 1–6.
[13] V. Pichapati and P. Gupta, “Practical considerations in cluster design for co-ordinated multipoint (CoMP) systems,” in 2013 IEEE International Conference on Communications (ICC), June 2013, pp. 5860–5865.
[14] A. Papadogiannis, D. Gesbert, and E. Hardouin, “A dynamic clustering approach in wireless networks with multi-cell cooperative processing,” in 2008 IEEE International Conference on Communications, May 2008, pp. 4033–4037.
[15] W. Saad, Z. Han, M. Debbah, and A. Hjorungnes, “A distributed coalition formation framework for fair user cooperation in wireless networks,” IEEE Transactions on Wireless Communications, vol. 8, no. 9, pp. 4580–4593, Sept 2009.
[16] V. Garcia, Y. Zhou, and J. Shi, “Coordinated multipoint transmission in dense cellular networks with user-centric adaptive clustering,” IEEE Transactions on Wireless Communications, vol. 13, no. 8, pp. 4297–4308, Aug 2014.
[17] Z. Zhang, N. Wang, J. Zhang, and X. Mu, “Dynamic user-centric clustering for uplink cooperation in multi-cell wireless networks,” IEEE Access, vol. 6, pp. 8526–8538, 2018.
[18] R. Wei, Y. Wang, and Y. Zhang, “A two-stage cluster-based resource management scheme in ultra-dense networks,” in 2014 IEEE/CIC International Conference on Communications in China (ICCC), Oct 2014, pp. 738–742.
[19] S. Tang, C. Sun, J. Wang, Y. Zhang, and F. Wen, “Interference management based on cell clustering in ultra-highly dense small cell networks,” in 2015 International Conference on Information and Communications Technologies (ICT 2015), Apr 2015, pp. 1–6.
[20] S. Chen, C. Xing, Z. Fei, H. Wang, and Z. Pan, “Dynamic clustering algorithm design for ultra dense small cell networks in 5G,” in 2015 10th International Conference on Communications and Networking in China (ChinaCom), Aug 2015, pp. 836–840.
[21] Z. Xiao, J. Yu, T. Li, Z. Xiang, D. Wang, and W. Chen, “Resource allocation via hierarchical clustering in dense small cell networks: A correlated equilibrium approach,” in 2016 IEEE 27th Annual International Symposium on Personal, Indoor, and Mobile Radio Communications (PIMRC), Sept 2016, pp. 1–5.
[22] W. Yao, J. Li, B. Tan, and S. Hao, “Interference management scheme of ultra dense network based on clustering,” in 2017 IEEE 2nd Information Technology, Networking, Electronic and Automation Control Conference (ITNEC), Dec 2017, pp. 374–377.
[23] P. Marsch and G. Fettweis, “Static clustering for cooperative multi-point (CoMP) in mobile communications,” in 2011 IEEE International Conference on Communications (ICC), June 2011, pp. 1–6.
[24] D. Gesbert, S. Hanly, H. Huang, S. Shamai (Shitz), O. Simeone, and W. Yu, “Multi-cell MIMO cooperative networks: A new look at interference,” IEEE Journal on Selected Areas in Communications, vol. 28, no. 9, pp. 1380–1408, Dec 2010.
[25] O. Simeone, N. Levy, A. Sanderovich, O. Somekh, B. M. Zaidel, H. V. Poor, and S. Shamai (Shitz), “Cooperative wireless cellular systems: An information-theoretic view,” Foundations and Trends® in Communications and Information Theory, vol. 8, no. 1–2, pp. 1–177, 2012.
[26] S. H. Park, O. Simeone, O. Sahin, and S. Shamai (Shitz), “Fronthaul compression for cloud radio access networks: Signal processing advances inspired by network information theory,” IEEE Signal Processing Magazine, vol. 31, no. 6, pp. 69–79, Nov 2014.
[27] O. Simeone, A. Maeder, M. Peng, O. Sahin, and W. Yu, “Cloud radio access network: Virtualizing wireless access for dense heterogeneous systems,” Journal of Communications and Networks, vol. 18, no. 2, pp. 135–149, Apr 2016.
[28] L. Zhou and W. Yu, “Uplink multicell processing with limited backhaul via per-base-station successive interference cancellation,” IEEE Journal on Selected Areas in Communications, vol. 31, no. 10, pp. 1981–1993, Oct 2013.
[29] “Hierarchical clustering with prototypes via minmax linkage,” Journal of the American Statistical Association, vol. 106, no. 495, pp. 1075–1084, 2011.
[30] D. Bertsekas, Nonlinear Programming. Athena Scientific, 1999.
[31] G. Calcev, D. Chizhik, B. Goransson, S. Howard, H. Huang, A. Kogiantis, A. F. Molisch, A. L. Moustakas, D. Reed, and H. Xu, “A wideband spatial channel model for system-wide simulations,” IEEE Transactions on Vehicular Technology, vol. 56, no. 2, pp. 389–403, March 2007.
[32] A. Y. Ng, M. I. Jordan, and Y. Weiss, “On spectral clustering: Analysis and an algorithm,” in Proceedings of the 14th International Conference on Neural Information Processing Systems: Natural and Synthetic, ser. NIPS’01. Cambridge, MA, USA: MIT Press, 2001, pp. 849–856.
[33] M. Yemini and A. J. Goldsmith, “‘Fog’ optimization via virtual cells in cellular network resource allocation,” in Arxiv. [eX:1901.06669, January 2019.]