Large magnetocaloric entropy change at room temperature in soft ferromagnetic manganites

Souhir Bouzidi,a Mohamed Amara Gdaiem, b* a J. Dhahri a and E. K. Hlil b

In this paper, La0.75Ca0.25xNa0.35MnO3 (x = 0.15 and 0.20) samples were prepared by the flux method. Crystallographic study revealed that the x = 0.15 sample is characterized by the coexistence of a mixture of orthorhombic and rhombohedral structures with Pbnm and R3c space groups, respectively. While, the x = 0.20 sample crystallized in the rhombohedral structure with a R3c space group. Magnetic data, under a magnetic field of 0.05 T, indicated that our samples undergo a ferromagnetic (FM)–paramagnetic (PM) phase transition, on increasing the temperature. The magnetic field dependence of the magnetocaloric properties of La0.75Ca0.25xNa0.35MnO3 (x = 0.15 and 0.20) samples, with the second phase transition, was investigated. Near room temperature, the x = 0.20 sample exhibited a large magnetic entropy change with maxima of 6.01 and 3.12 J kg⁻¹ K⁻¹, respectively, under applied magnetic fields of 5 and 2 T. Also, the relative cooling power (RCP) was calculated. According to hysteresis cycles, for our studied samples, at 10 K a typical soft FM behavior with a low coercive field was observed. These results make our samples promising candidates for magnetic refrigerators, magnetic recording, and memory devices.

1. Introduction

During the past few years, perovskite manganites with a general formula Ln₁₋ₓMMnO₃ (where Ln is a rare earth element and M is a divalent alkaline ion) have attracted particular attention from several researchers. This is thanks to their interesting interplay between magnetic and electronic features, as well as to being very promising for future technological applications.1–7 Additionally, they have many advantages such as low production cost, convenient preparation, softer vibration, longer usage time, small volume requirement and chemical stability. Moreover, these materials are environment-friendly and do not cause noise pollution. This makes them attractive to further research in relation to the widely-used refrigeration technology based on gas compression. The parent compound, LnMnO₃, is an antiferromagnetic (AFM)-insulator characterized by a superexchange (SE) coupling between Mn³⁺ ions. When the Ln site is substituted with a divalent ion, a proportional number of Mn¹⁺ ions with the electronic configuration (3d⁴, t₂g↑ e_g↑, S = 2) are converted into Mn⁴⁺ ions with the electronic configuration (3d⁴, t₂g↑ e_g↓ S = 3/2). This mixed Mn¹⁺/Mn⁴⁺ valence gives rise to a double exchange (DE) transfer of eg electrons from Mn¹⁺ to Mn⁴⁺ ion via the O²⁻ ion network. DE plays an important role in the properties of these materials.8 These properties are very dependent on the substitution rate x, average size of the cation, cationic disorder and the elaboration method.9 La₁₋ₓCaₓMnO₃ has attracted the attention of several researchers. This is thanks to the very rich phase diagram observed in this series.10–12 Pekala et al.13 investigated its magnetic field dependence of electrical resistivity in fine grains and analyzed the influence of external magnetic field on the transport processes in detail. Yi et al.14 observed that the magnetoresistance of nanosized La₀.₇5₋ₓCa₀.₂₅ₓNaₓMnO₃ is enhanced at low temperatures due to the spin-polarized tunneling behavior. In addition, the pressure dependence of magnetic phase separation and transport behavior in La₀.₇5₋ₓCa₀.₂₅ₓNaₓMnO₃ has also been investigated in recent paper.15 On other hand, with the substitution of Na on LaMnO₃ sample, an amount 2x of Mn³⁺ is converted to Mn⁴⁺. Zhong et al.16 have studied the magnetocaloric properties in La₁₋ₓNaₓMnO₃ (0 ≤ x ≤ 0.2) and found that for x = 0.2, |ΔS_M|max reaches 1.96 J kg⁻¹ K⁻¹ upon a magnetic applied field change of 1 T. This paper investigates the effect of Na substitution on the structural, magnetic and magnetocaloric effect (MCE) of (x = 0.15 and 0.20) samples, synthesized by flux method, using sodium chloride (NaCl) as a flux. A theoretical investigation was used to predict the MCE properties for x = 0.20.

2. Experimental details

Generally, ceramic materials are highly affected by the preparation routes and heat treatments. The synthesis methods based on the conventional ceramic or solid state reaction are not suitable for advanced technological applications, as these methods produce particles of large size at high temperatures.
Alternatively, to produce a very high-quality, homogenous and nano-polycrystalline powder of La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x = 0.15$ and $0.20$) compounds, at low temperature, we used the flux method, NaCl as a flux. The scheme of the synthetic route is to take stoichiometric amounts of high purity La$_2$O$_3$, MnO$_2$ and CaCO$_3$ in the appropriate molar ratio. The last mixture was ground, for half an hour, with an appropriate quantity of NaCl in an agate mortar. Then, the mixture was heated at 800 °C for 24 h in a recrystallized alumina crucible. After that, the melt was washed with distilled water and filtrated in order to remove easily the residual salts. The resulting powder was dried at 110 °C for 3 h and heated at 800 °C for 6 h. Finally, the powder was pressed into disks under 5 tonnes per cm$^2$ and sintered at 800 °C. In order to characterize our samples, we carried out XRD analysis with CuK$_\alpha$ radiation. The data were analyzed by Rietveld method using Fullprof program. Fig. 1(a) and (b) exemplifies the Rietveld refinement of XRD profile, for the $x = 0.15$ and $0.20$ samples, respectively. A}

![Image of XRD patterns](image_url)

**3. Results and discussion**

**3.1 X-Ray diffraction study**

To analyze the structural properties of our samples, we carried out XRD analysis with CuK$_\alpha$ radiation at room temperature. The data were analyzed by Rietveld method using Fullprof program. Fig. 1(a) and (b) exemplifies the Rietveld refinement of XRD profile, for the $x = 0.15$ and $0.20$ samples, respectively. A
good agreement between the observed and the calculated profiles was remarked. This is due to the excellent goodness of fit (χ²), confirming the high quality of refinement. From this figure, we can deduce that the x = 0.15 sample is a mixture of orthorhombic and rhombohedral structures, respectively, with Pbnm and R3c space groups, around 2θ = 32°. In this region, the system showed a sign of multi-phased behavior with no complete splitting into the double line of the intense peak. This result is in concordance with that observed in ref. 18. The relative amount of the orthorhombic phase was 81.68%. We can see the appearance of a small quantity of Mn₃O₄, as found in recent works.19,20

The different fitting parameters of our samples are summarized in Table 1. According to Shannon,21 the ionic radius of Na⁺ (r_{Na⁺} = 1.24 Å) is higher than that of Ca²⁺ (r_{Ca²⁺} = 1.18 Å). This can be explained by the slight increase of the lattice size with increasing Na content. It has been reported that the deformation of the MnO₆ octahedron may be responsible for the distortion in the perovskite structures. The crystal structure with a uniform grain size distribution, for x = 0.15 as an example, was remarked. This is due to the excellent goodness of fit (χ²).

### Table 1: Refined structural parameters for La_{0.75}Ca_{0.25−x}NaₓMnO₃ (x = 0.15 and 0.20) samples determined from X-ray after the Rietveld refinement at room temperature

| Parameter | x = 0.15 | x = 0.20 |
|-----------|----------|----------|
| Space group | Pbnm | R3c |
| a (Å) | 5.502(3) | 5.482(4) |
| b (Å) | 5.461(5) | 5.482(4) |
| c (Å) | 7.751(8) | 13.406(3) |
| V (Å³) | 232.963 | 348.975 |
| La/Ca/Na | |
| x | 0.498(8) | 0.0000 |
| y | 0.013(1) | 0.0000 |
| z | 0.2500 | 0.2500 |
| B_{iso} (Å²) | 1.16(6) | 1.08(2) |
| Mn | |
| B_{iso} (Å²) | 0.66(2) | 0.68(4) |
| O₁ | |
| x | 0.226(7) | 0.443(8) |
| y | 0.306(5) | 0.0000 |
| z | 0.008(9) | 0.2500 |
| B_{iso} (Å²) | 1.45(2) | 1.51(3) |
| O₂ | |
| x | 0.576(8) | — |
| y | 0.496(6) | — |
| z | 0.2500 | — |
| B_{iso} (Å²) | 1.41(5) | — |
| Discrepancy factors | |
| R_p (%) | 4.38 | 4.05 |
| R_wp (%) | 5.82 | 5.16 |
| χ² | 1.81 | 1.40 |
| Bond lengths and bond angles | |
| d_{Mn-O-Mn} (Å) | |
| d_{Mn-O} (Å) | |
| Bandwidth W (10⁻²) (u.a.) | 8.1 | 9.3 |
| Tolerance factor T_G | 0.9758 | 0.9795 |

The XRD density (D_{XRD}) of our samples is determined from X-ray measurements.24 It was found to be 5.963 and 5.958 g cm⁻³, respectively, for x = 0.15 and 0.20 samples.

### 3.2 Morphological study

From the reflection of 2θ values of XRD profile, the crystallite size (D) was calculated using Scherrer’s equation (eqn (2)):

\[ D = \frac{K \lambda}{\beta \cos(\theta)} \tag{2} \]

where K is the shape factor, which usually takes a value of about 0.9, λ = 1.5406 Å is the wavelength for CuKα radiation, θ is the diffraction angle of the most intense peak and β is the full width at half maximum of the highest peak. D values are listed in Table 2. The obtained values are comparable with those reported in the literature.26–28 Regarding the SEM micrograph, insets (a) and (b) of Fig. 2, show a homogenous microstructure and a uniform grain size distribution, for x = 0.15 as an example. The grain sizes were estimated to be mostly within 2.12 and 2.14 µm for x = 0.15 and 0.20, respectively. Obviously, the particle sizes observed by SEM were much larger than those calculated using Scherer’s formula. This indicates that each grain observed by SEM consists of several crystallites.31–33

In order to check the existence of all elements in La_{0.75}Ca_{0.25−x}NaₓMnO₃ (x = 0.15 and 0.20) compounds, EDX analysis was performed. The EDX spectrum, for x = 0.15 as an example, is shown in Fig. 2. The typical cationic compositions are listed in Table 3. It is clear that all elements (La, Ca, Na, Mn, and O) structures and the MnO₆ octahedron for the samples (x = 0.15 and 0.20) were drawn using the VESTA program (inset of Fig. 1(a) and (b)).22 To better understand the regularities governing the formation of perovskite-type systems, Goldschmidt’s tolerance factor, T_G, is usually introduced. It is defined by the following expression:

\[ T_G = \frac{\langle r_{(La, Ca, Na)} \rangle + \langle r_O \rangle}{\sqrt{2(r_{Mn} + \langle r_O \rangle)}} \tag{1} \]

where \(r_{(La, Ca, Na)}\), \(r_O\) and \(r_{Mn}\) are the ionic radii of the different elements. The manganese oxide compounds have a perovskite structure if 0.89 < T_G < 1.02.25 The obtained values of T_G for our samples were listed in Table 1. This confirmed the stability of this structure.

The experimental density (D_{exp}) is determined from the weight and geometrical dimensions of the cylindrical pellets.26 It was found to be 5.963 and 5.958 g cm⁻³, respectively, for x = 0.15 and 0.20 samples.
are present with no loss of any integrated elements during the sintering process.

3.3 Magnetic study

Following the Morphological study, we discussed the thermal variation of the magnetic properties of La_{0.75}Ca_{0.25}Na_{x}MnO_{3} (x = 0.15 and 0.20). Fig. 3(a) and (b) shows the zero-field-cooled (ZFC) and field-cooled (FC) magnetizations of our samples under an applied field of 0.05 T in the temperature range 5 to 400 K. We can remark a net PM–FM transition, at their T_C. A small divergence between ZFC and FC plots can be observed at the irreversibility temperature T = 270 and 250 K, respectively for x = 0.15 and 0.20. This phenomenon can be attributed to the appearance of an isotropic field generated from FM clusters. At low temperatures, a small peak was observed around 40 K. This indicates the appearance of Mn_{3}O_{4} phase. T_C can be determined from d^{2}M/dT^{2} graphs (Fig. 3(a) and (b)). From this figure, we remarked the appearance of different inflection points. For the x = 0.20 sample, a classical behavior at 300 K was observed, corresponding to its T_C. While the x = 0.15 sample presented two inflection points, around room temperature, corresponding to two Curie temperatures. This can be interpreted by the presence of two different FM phases. The Curie temperatures were measured at T_{C1} = 273 K and T_{C2} = 301.5 K. Additionally, we can see a slight decrease of T_C with increasing Na+ content. According to Asma Zaidi et al., the decrease of T_C can be interpreted in terms of the increase in Mn^{4+} content above 40%, which produces a decrease in the DE interaction (Mn^{3+}–O^{2−}–Mn^{4+}) and enhances the SE interaction (Mn^{4+}–O^{2−}–Mn^{4+}). Here, we can discuss the evolution of the bandwidth using eqn (3)

$$W_b \approx \frac{\cos \omega}{d_{(\text{Mn-O})}^{15}},$$

where \(\omega = 1/2(\pi - (\text{Mn-O-Mn}))\) and \(d_{(\text{Mn-O})}\) is the bond length characterized by the overlap between Mn_{3d} and O_{2p} orbitals. The calculated \(W_b\) values are tabulated in Table 1.

To understand the dynamics of spin, we carried out the inverse of susceptibility as function of temperatures, as shown in Fig. 4. In PM region, \(\chi^{-1}\) can be fitted by Curie–Weiss (CW) law.

### Table 3 Results of EDX analysis

| Nominal composition | Typical cationic composition from EDX |
|---------------------|-------------------------------------|
| La_{0.75}Ca_{0.25}Na_{x}MnO_{3} | 0.751 0.101 0.149 1.000 |
| La_{0.75}Ca_{0.05}Na_{x}MnO_{3} | 0.750 0.049 0.201 1.001 |

Fig. 2 The EDX analysis for x = 0.15 sample. Insets: (a) shows the typical SEM and (b) shows the histogram of the distribution of particle size.
by the magnetic inhomogeneity above $T_C$. The experimental effective moment ($m_{\text{eff}}^{\text{exp}}$) and the theoretical effective moment ($m_{\text{eff}}^{\text{theo}}$) are also calculated. The obtained values of $m_{\text{eff}}^{\text{exp}}$ and $m_{\text{eff}}^{\text{theo}}$ are listed in Table 4. We can notice that the difference between the experimental and the theoretical values is attributed to the FM correlations in PM region. These are probably due to the formation of FM cluster. Our results are comparable with other works. In addition, it is important to mention that the percentage of Mn$^{3+}$ and Mn$^{4+}$ ions can be checked quantitatively by the so-called chemical titration. To verify these percentages, we carried out a chemical analysis. In fact, our obtained powder was dissolved in concentrated sulfuric acid and oxalic acid dihydrate. The obtained solution is titrated by potassium permanganate and the values of manganese ions concentration are (Mn$^{3+}$ = 60.1%) and (Mn$^{4+}$ = 39.9%) for $x$ = 0.15 and (Mn$^{3+}$ = 54.8%) and (Mn$^{4+}$ = 45.2%) for $x$ = 0.20. In order to get a deeper insight into the magnetic properties at low temperatures, we analysed the hysteresis cycles $M(\mu_0H)$. Fig. 5(a) and (b) displays $M(\mu_0H)$ at 0 K, $\mu_0H = \pm 6$ T. We remarked clearly that the curves are quite similar to each other with a small hysteresis loop. In the weak field region at low

### Table 4: Some experimental values for La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x$ = 0.15 and 0.20) compounds

| $x$  | $T_C$ (K) | $\theta_0$ (K) | $\mu_{\text{eff}}^{\text{theo}}$ ($\mu_B$) | $\mu_{\text{eff}}^{\text{exp}}$ ($\mu_B$) |
|------|-----------|---------------|---------------------------------|---------------------------------|
| 0.15 | 301.5     | 301, 66       | 4.51                            | 5.62                            |
| 0.20 | 300       | 301, 11       | 4.46                            | 5.33                            |

Fig. 3 Temperature dependence of the ZFC and FC magnetization and $d^2M/dT^2$ plots for La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x$ = 0.15 and 0.20) compounds, under a magnetic field of 0.05 T.

Fig. 4 Inverse of susceptibility as a function of temperatures for La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x$ = 0.15 and 0.20) samples determined in a field of 0.05 T.

Fig. 5 Magnetic hysteresis cycles at $T = 10$ K of La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x$ = 0.15 and 0.20) samples. The insets show a zoom of the central portion of the hysteresis at a low field.
temperatures, magnetization increased significantly and reached saturation upon increasing field. The saturation magnetization \((M_s)\) was found to be 88.10 and 92.21 emu g\(^{-1}\), for \(x = 0.15\) and \(x = 0.20\), respectively. The insets of Fig. 5(a) and (b) show a zoom of the central portion, at low magnetic fields, of \(M(\mu_0 H)\) curves. It is clear that \(M(\mu_0 H)\) curves have negligible values of coercive field \((\mu_0 H_C)\) and remnant magnetization \((M_r)\). \(\mu_0 H_C\) values are found to be \(21 \times 10^{-4}\) and \(16 \times 10^{-4}\) T, for \(x = 0.15\) and \(x = 0.20\), respectively. \(M_r\) values were found to be 1.49 and 1.11 emu g\(^{-1}\), for \(x = 0.15\) and \(x = 0.20\) respectively. The small hysteresis loop with important saturation values indicates the typical soft FM behavior of materials. According to these results, our samples could be used for reading and writing process in high density recording media or information storage.

Magneto-crystalline anisotropy is an intrinsic property of materials, playing an important role in coercivity.\(^{43}\) It is used to describe the effect of the internal energy on the direction of magnetization.

According to Stoner–Wohlfarth’s theory, the anisotropy constant \((K_a)\) can be determined from eqn (4)\(^44\)

\[
\mu_0 H_C = (0.98 \times K_a)/M_S, \tag{4}
\]

where \(K_a\) values are 188.7 J m\(^{-3}\) and 161.9 J m\(^{-3}\), for the \(x = 0.15\) and \(x = 0.20\) samples, respectively.

The remanence ratio \((R)\) using (eqn (5)):

\[
R = M_r/M_S \tag{5}
\]

is an important parameter, used to understand the isotropic nature of our studied samples. \(R\) values are equal to 0.0169 and 0.0120, for the \(x = 0.15\) and \(x = 0.20\) samples, respectively. The small obtained values undergo the isotropic nature.\(^{45}\) Together with \(M(\mu_0 H)\) investigation; we have measured the isothermal magnetization as a function of applied magnetic fields up to 5 T at different temperatures, for our samples, around their \(T_C\) (inset of Fig. 6(a) and (b)). We can notice that these curves reveal a rapid increase in the magnetization at a very weak magnetic field corresponding to a quick rearrangement of the magnetic domains. This is due to the complete alignment of the spins in these samples from the value of the magnetic field, 1 T. To clarify the nature of the magnetic phase transition, we derived the Arrott’s plots \((M^2 \text{ vs. } \mu_0 H/M)\) from \(M(\mu_0 H)\). The obtained curves are shown in Fig. 6(a) and (b), for the \(x = 0.15\) and \(x = 0.20\) samples. According to Banerjee’s criterion, a positive slope corresponds to second order magnetic transition, while a negative slope corresponds to first order transition.\(^{46}\) From Fig. 6(a) and (b), we can see a positive slope without inflection points in the high-field regions for our samples. This indicates that our samples undergo a second order nature of phase FM–PM transition.

### 3.4 Magnetocaloric properties

For the determination of MCE especially in magnetic materials, both the experimental and theoretical approaches are used. However, for the theoretical investigation of MCE, several approaches were used. Recently, a theoretical model proposed by Hamad\(^{47}\) began to receive attention. Based on this model, the dependence of magnetization on the temperatures is defined as:

\[
M = \left(\frac{M_f - M_i}{2}\right) \tanh[A(T_C - T)] + BT + C \tag{6}
\]

where \(M_i\) and \(M_f\) are the initial and the final values of magnetization at FM–PM transition, respectively. \(A = \frac{2(B - S_C)}{M_f - M_i}\). \(B\) is the magnetization sensitivity \(dM/dT\) at FM state before transition. \(S_C\) is the magnetization sensitivity \(dM/dT\) at \(T_C\).

\[
C = \left(\frac{M_f - M_i}{2}\right) - BT_C. \tag{7}
\]

According to this model, \(\Delta S_M\) under applied magnetic fields in the range of 0 to \(\mu_0 H_{\text{max}}\) is expressed by:\(^{48}\)

\[
\Delta S_M(T) = \left(A \left(\frac{M_f - M_i}{2}\right) \text{sech}^2(A(T_C - T)) - B\right)\mu_0 H_{\text{max}} \tag{7}
\]

At \(T = T_C\), we obtained \(\Delta S_M^{\text{max}}\) value, defined as the following expression:\(^{48}\)

\[
\Delta S_M^{\text{max}} = \left(A \left(\frac{M_f - M_i}{2}\right) - B\right)\mu_0 H_{\text{max}} \tag{8}
\]
In magnetic refrigeration, it is important to take into account not only the $-\Delta S_M$, but also the relative cooling power (RCP) as an important parameter which represents the amount of heat exchange per kilogram between the hot and cold sinks in the ideal refrigeration cycle. It is computed by:\(^{(50)}\)

$$\text{RCP} = -\Delta S_M^{\text{max}} \times \delta T_{\text{FWHM}}$$

$$= \left[ M_t - M_f - \frac{2B}{A} \right] \mu_0H_{\text{max}} \times \text{sech} \left( \frac{2A(M_f - M_t)}{A(M_t - M_f) + 2B} \right)$$

$$\delta T_{\text{FWHM}}$$ presents the full width at half maximum, defined as:\(^{(58)}\)

$$\delta T_{\text{FWHM}} = \frac{2}{A} \cosh^{-1} \left( \frac{2A(M_f - M_t)}{A(M_t - M_f) + 2B} \right)^{1/2}$$

Another important parameter for magnetic refrigeration is the heat capacity $\Delta C_{P,\mu H}$ associated with an applied magnetic field (1–5 T) can be determined by:

$$\Delta C_{P,\mu H} = T \frac{\delta \Delta S_M}{\delta T}$$

$$\Delta C_{P,\mu H}$$ can be rewritten as:\(^{(51)}\)

$$\Delta C_{P,\mu H} = -TA^2(M_t - M_f) \times \text{sech}^2[A(T_C - T)] \tanh[A(T_C - T)]$$

$$\mu_0H_{\text{max}}$$

In the rest of our work, the MCE properties for $x = 0.15$ will be determined experimentally, while $x = 0.20$ will be determined experimentally and theoretically.

Before studying the MCE properties of our samples, Fig. 7 represents $M(T)$ in different applied magnetic field, for $x = 0.20$ sample. The symbol is the experimental data, while the solid red line is the modeled data (using eqn (6)). From $M(T)$, it is easy to determine $M_t$, $M_f$, $B$ and $S_C$ parameters in order to investigate theoretically $-\Delta S_M$, RCP, $-\Delta C_{P,\mu H}$ and $\Delta T_{\text{ad}}$ curves. The obtained parameters are summarized in Table 5.

It is noteworthy that the theoretical model is in good agreement with the experimental data.

Fig. 8(a) and (b) shows the variation of $-\Delta S_M$ as a function of temperature, under applied magnetic fields of 1–5 T, for the $x = 0.15$ and 0.20 samples, respectively. For the $x = 0.20$ sample, it is clear that the theoretical results (using eqn (7)) are consistent with the experimental results. This confirms the validity of this model. From Fig. 8, we can see a positive sign of $-\Delta S_M$ in the entire temperature range, confirming the FM character. Around $T_C$, the $x = 0.20$ sample exhibited a classical behavior of $-\Delta S_M$ with a maximum peak of 6.01 J kg$^{-1}$ K$^{-1}$ under $\mu_0H = 5$ T field. While, for the $x = 0.15$ sample, we remarked the coexistence of two peaks. This corresponds to two Curie temperatures. When studying the effect of Ag$^+$ in the La$_{0.5}$Ca$_{0.5}$MnO$_3$ sample, Kalyana et al. have shown that the $x = 0.10$ sample admits two magnetic transitions. This can be due to the existence of Curie phase in the FM matrix.\(^{(52)}\) A. Krichene et al. have shown that the La$_{0.6}$Gd$_{0.1}$Ca$_{0.3}$MnO$_3$ and La$_{0.6}$Eu$_{0.1}$Ca$_{0.3}$MnO$_3$ samples admit two maxima of $-\Delta S_M$. The first one corresponds to $T_C$. While, the second one is an anomaly, which explained as magnetic transition: in fact, PM and AFM transitions coexist above $T_C$.\(^{(53)}\) Hence, in our case the presence of two peaks in $-\Delta S_M$ may be attributed to the combination of orthorhombic and rhombohedral structures in this sample. This is in agreement with that observed by Kima et al.\(^{(54)}\) The obtained $-\Delta S_M^{\text{max}}$ are comparable with those obtained in the literature (Table 6).

The different values of RCP for our samples are listed in Table 6. These parameters increase with increasing the external magnetic field. This is because the effect of spin coupling became less important when the applied magnetic field was increased. We can see that the proposed compounds exhibit important values. In addition, we can note that our samples can be considered as potential candidates for magnetic refrigeration thanks to their high RCP values, compared to conventional refrigerative materials (Table 6).

Using eqn (11) and (12), Fig. 9 display the experimental and the theoretical $-\Delta C_{P,\mu H}$ plots, for $x = 0.20$ sample as an example. The symbol represents the experimental data, while the solid red line represents the modeled data. We can see clearly that the experimental results are in a good agreement with the calculated results. Additionally, we can remark that the value of $-\Delta C_{P,\mu H}$ suddenly changed from positive to negative around $T_C$. Then, it decreased rapidly with decreasing temperature.\(^{(55)}\) The sum of the two parts represents the magnetic contribution to the total specific heat. The positive or negative values of $\Delta C_{P,\mu H}$ can strongly alter the heating or cooling power of a magnetic refrigerator. The obtained maximum/minimum values of $\Delta C_{P,\mu H}$ at 315/293 K, exhibited an increasing trend with the external magnetic field. It was found to be 63.98/–62.62 J kg$^{-1}$ K$^{-1}$ at a 5 T applied magnetic field. Our results are comparable with those obtained in recent works.\(^{(4)}\)

To have a wider understanding of the MCE properties, the adiabatic temperature change ($\Delta T_{\text{ad}}$) was calculated. It is defined as following:\(^{(51)}\)
Table 5  Model parameters for La$_{0.75}$Ca$_{0.25}$MnO$_3$ $(x = 0.15$ and $0.20$) compounds in different applied magnetic fields

| $\mu_0 H$ (T) | $M_1$ (emu g$^{-1}$) | $M_2$ (emu g$^{-1}$) | $B$ (emu g$^{-1}$ K$^{-1}$) | $S_C$ (emu g$^{-1}$ K$^{-1}$) | $T_C$ (K) |
|---|---|---|---|---|---|
| 1 | 49.60 | 11.25 | −0.204 | −1.772 | 299.97 |
| 2 | 53.75 | 16.17 | −0.233 | −1.597 | 301 |
| 3 | 58.66 | 22.73 | −0.247 | −1.365 | 301.65 |
| 4 | 62.48 | 31.39 | −0.294 | −1.321 | 302.13 |
| 5 | 63.59 | 34.57 | −0.303 | −1.286 | 303.45 |

\[
\Delta T_{ad}(T, \Delta \mu_0 H) = \frac{T}{C_{P, ad} H} \int_{T_{ad}}^{T_{ad}} \frac{\partial M}{\partial T} d\mu_0 H = -\frac{T}{C_{P, ad} H} \Delta S_M \tag{13}
\]

\[
\Delta T_{ad}(T, \Delta H) = \mu_0 H_{max} = AT \left( \frac{M_1 - M_2}{2C_{P, ad} H} \right) \left( \text{sech}^2(A(T_C - T)) + B \right) \mu_0 H_{max} \tag{14}
\]

\[C_{P, ad} H \] represents the specific heat, it can be calculated from the sum of the lattice and magnetic contributions using eqn (15)$^{66,67}$

\[C_{P, H} = C_D + C_M. \tag{15}\]

where $C_D$ is the Debye specific heat and $C_M$ is the magnetic contribution to the specific heat capacity. $C_M$ is given by $(\partial U_M/\partial T)$, and is determined from$^{66,67}$

\[C_M = -H_{ad} \frac{\partial M}{\partial T} - \frac{1}{2} N_{int} \frac{\partial M^2}{\partial T^2}, \tag{16}\]

where $N_{int}$ presents the mean field constant. It is equal to

\[\frac{3KT_C}{N_S g^2 \mu_0^2 J(j+1)}, \]

$g$ is the Landé factor, $J$ is the total angular momentum and $N_S$ is the number of spins per unit mass.

Using eqn (13) and (14), Fig. 10(a) and (b) shows the experimental and theoretical curves of $\Delta T_{ad}$ for our samples, respectively. The symbol represents the experimental data, while the solid red line refers to the modeled data. It is obvious that the results of calculation are in good agreement with the experimental results. Also, it is clear that $\Delta T_{ad}$ maintains practically the nature of $-\Delta S_M$. The maximum values of $\Delta T_{ad}$ range from 2.93 and 3.64 K at 5 T, for $x = 0.15$ and 0.20, respectively.

A phenomenological universal curve for the field dependence of $-\Delta S_M$ has been proposed, by Franco et al.$^{66}$ It is based on the normalization of all $-\Delta S_M(T, \mu_0 H)$ curves using eqn 17

\[-\Delta S' = \Delta S_M(T, \mu_0 H)/\Delta S_M^{\text{max}}. \tag{17}\]

After that, the temperatures' axes are differently rescaled below and above $T_C$, defined as (eqn (18))$^{69}$

\[\theta = \begin{cases} 
\frac{T - T_C}{T_C - T_{t_1}} & T \leq T_C \\
\frac{T - T_C}{T_{t_2} - T_C} & T > T_C 
\end{cases} \tag{18}\]

where, $T_{t_1}$ and $T_{t_2}$ are the temperatures of two reference points, associated to $\Delta S_M(T_{t_1}) = -\Delta S_M^{\text{max}}/2 (T_{t_1} < T_C$ and $T_{t_2} > T_C)$. Fig. 11 displays the $\theta$ dependence of $\Delta S'$ under different magnetic fields, for the $x = 0.20$ sample, as an example. It is clearly seen that all data points collapse on one single curve. Therefore, the FM–PM phase transition in our sample was confirmed to be of second order nature.$^{68}$

The universal curve can be well fitted by Lorentz’s function using (eqn (19))

\[-\Delta S' = \frac{a}{b + (\theta - c)^2} \tag{19}\]
where $a$, $b$, and $c$ are free parameters. Taking into consideration the asymmetry of the curves (for $x = 0.20$ as an example), we can use two different regions of constants such as: for $T < T_C$ region, $a = 1.458 \pm 0.037$, $b = 1.391 \pm 0.026$ and $c = 0.174 \pm 0.021$. While, for $T > T_C$ region, $a = 0.717 \pm 0.046$; $b = 0.743 \pm 0.048$ and $c = 0.122 \pm 0.030$. Our obtained parameters are comparable to those obtained in ref. 71. According to eqn (19), only the different parameters namely $T_C$, $-\Delta S_M^{\text{max}}$, $T_1$, and $T_2$ values are needed to characterize $-\Delta S_M$. That is to say, we need only the last parameters, which are determined from the properties of these materials, to determine $-\Delta S_M$ from $\Delta S'(\theta)$.

Generally, $-\Delta S_M$ is dependent on the variation of magnetization near $T_C$. It can be expressed by:

$$\Delta S_M(T, \mu_0H) = a(T)(\mu_0H)^n$$

(20)

where $n$ is an exponent which depends on the magnetic transition and defined as:

$$n(T, \mu_0H) = \frac{d \ln(|\Delta S_M|)}{d \ln(\mu_0H)}$$

(21)

Fig. 12 displays the variation of $n$ as function of temperatures, under different applied fields, for the $x = 0.20$ sample. We can see that the value of $n$ approaches 1 in the FM region and admits a minimum in $T_C$. Then, it approaches 2 in the PM state. These results are observed in different magnetic materials.74-76

Table 6 Summary of MC properties of La$_{0.75}$Ca$_{0.25-x}$Na$_x$MnO$_3$ ($x = 0.15$ and 0.20) compounds compared with other works

| Samples                        | $T_C$ (K) | $\mu_0H$ (T) | $-\Delta S_M^{\text{max}}$ (J kg$^{-1}$ K$^{-1}$) | RCP (J kg$^{-1}$) | Ref.
|--------------------------------|-----------|--------------|-----------------------------------------------|-----------------|-------
| La$_{0.75}$Ca$_{0.10}$Na$_{0.15}$MnO$_3$ | 301.5     | 5            | 4.83                                          | 230             | Present work
| La$_{0.75}$Ca$_{0.10}$Na$_{0.15}$MnO$_3$ | —         | 2            | 2.33                                          | 110             | Present work
| La$_{0.75}$Ca$_{0.05}$Na$_{0.20}$MnO$_3$ | 300       | 5            | 6.01                                          | 225             | Present work
| La$_{0.75}$Ca$_{0.05}$Na$_{0.20}$MnO$_3$ | —         | 2            | 3.12                                          | 90              | Present work
| La$_{0.75}$Sm$_{0.05}$Sr$_{0.05}$Na$_{0.95}$MnO$_3$ | 294       | 5            | 4.50                                          | 193.48          | 55    |
| La$_{0.75}$Sm$_{0.05}$Sr$_{0.05}$Na$_{0.95}$MnO$_3$ | 294       | 2            | 2.80                                          | 97.30           | 55    |
| La$_{0.60}$Ba$_{0.15}$MnO$_3$ | 314       | 5            | 3.24                                          | 307             | 56    |
| Gd | 293 | 2 | 5 | 153 | 57 |
| Gd | 293 | 5 | 9.5 | 410 | 58 |
| La$_{0.57}$Nd$_{0.03}$Sr$_{0.12}$Mn$_{0.85}$O$_3$ | 281 | 5 | 2.8 | 51 | 59 |
| La$_{0.52}$Sr$_{0.15}$Mn$_{0.85}$O$_3$ | 308 | 2 | 2.2 | 90 | 60 |
| La$_{0.50}$Ba$_{0.20}$MnO$_3$ | 295 | 5 | 4.5 | 130 | 61 |
| La$_{0.50}$Sr$_{0.15}$Mn$_{0.85}$Fe$_{0.05}$O$_3$ | 260 | 2 | 1.7 | 83 | 62 |
| La$_{0.52}$Sr$_{0.15}$Ca$_{0.23}$MnO$_3$ | 294 | 2 | 3.72 | 149.43 | 63 |
| La$_{0.52}$Ca$_{0.25}$Sr$_{0.15}$MnO$_3$ | 308 | 5 | 7.45 | 374 | 64 |

Fig. 9 Experimental and theoretical curves of $\Delta C_P$ versus temperatures for $x = 0.20$ compounds under different magnetic fields.

Fig. 10 $\Delta T_{pd}$ plotted as a function of temperature at different $\mu_0H$ fields, for $x = 0.15$ and 0.20 compounds. The red line curves represent the modeled data and symbols are the experimental data.


In summary, we have investigated the structural, morphological, magnetic and MCE properties of La$_{0.75}$Ca$_{0.25}$–xNa$_x$MnO$_3$ ($x = 0.15$ and 0.20) samples, synthesized using the flux method. Rietveld refinement of XRD patterns shows that $x = 0.20$ crystallized in a rhombohedral structure with $R3c$ space group, at room temperature. While, the $x = 0.15$ sample admits both phases with different percentages. Magnetization measurements as function of temperatures in a magnetic field of 0.05 T show that our studied samples undergo a second-order PM-FM phase transition, upon decreasing temperature. Around room temperature, a large MCE is observed for our samples, under a magnetic field of 5 T. $\Delta S_{M}^{\text{max}}$ is found to be $6.01 \text{ J kg}^{-1} \text{ K}^{-1}$ under $\mu_0 H = 5$ T magnetic field for $x = 0.20$. For the $x = 0.15$ sample, $-\Delta S_{M}$ curves show the existence of two maxima, which may be attributed to the structural inhomogeneity. The RCP is also analyzed. From, $-\Delta S_{M}$ curves, we have investigated the dependence of temperature on the adiabatic temperature change ($-\Delta T_{ad}$). Its maximum is found to be 2.93 K, for the $x = 0.15$ sample, in an applied magnetic field of 5 T. From the hysteresis cycles, at 10 K for the studied samples, we can remark a typical soft FM behavior with a small hysteresis loop and a low coercive field ($\mu_0 H_C$). The small values of coercive field confirm that the magnetic domains can rotate easily to the direction of the applied magnetic field. These results make our samples promising candidates for magnetic refrigeration, magnetic recording and memory devices.

**Conflicts of interest**

The authors declare that they have no conflict of interest.

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