Inelastic quarkonium photoproduction in coherent hadron - hadron interactions at LHC energies

V.P. Gonçalves\textsuperscript{a} and M.M. Machado\textsuperscript{b}

\textsuperscript{a} Instituto de Física e Matemática, Universidade Federal de Pelotas
Caixa Postal 354, CEP 96010-900, Pelotas, RS, Brazil, and
\textsuperscript{b} Instituto Federal de Educação, Ciência e Tecnologia, IF - Farroupilha, Campus São Borja
Rua Otávio Costilho Mendes, 355, CEP 97670-000, São Borja, RS, Brazil.

In this paper we study the inelastic quarkonium photoproduction in coherent pp/pPb/PbPb interactions. Considering the ultra relativistic hadrons as a source of photons, we estimate the total $h_1 + h_2 \rightarrow h \otimes V + X$ ($V = J/\Psi$ and $\Upsilon$) cross sections and rapidity distributions at LHC energies. Our results demonstrate that the experimental analysis of this process can be used to understand the underlying mechanism governing heavy quarkonium production.

PACS numbers: 12.40.Nn, 13.85.Ni, 13.85.Qk, 13.87.Ce

I. INTRODUCTION

In the last years, the analysis of coherent hadron-hadron collisions becomes an alternative way to study the theory of strong interactions - the Quantum Chromodynamics (QCD) - in the regime of high energies (For a review see Ref. \cite{1}). The basic idea in coherent hadronic collisions is that the total cross section for a given process can be factorized in terms of the equivalent flux of photons in the hadron projectile and the photon-photon or photon-hadron production cross section. The main advantage of using colliding hadrons and nuclear beams for studying photon induced interactions is the high equivalent photon energies and luminosities, that can be achieved at existing and future accelerators. In particular, the photon-hadron interactions can be divided into exclusive and inclusive reactions. In the first case, a certain particle is produced, while the target remains in the ground state (or is only internally excited). On the other hand, in inclusive interactions the particle produced is accompanied by one or more particles from the breakup of the target. The typical examples of these processes are the exclusive vector meson production, described by the process $\gamma h \rightarrow V h$ ($V = J/\Psi$ and $\Upsilon$), and the inclusive heavy quark production $\gamma p \rightarrow XY$ ($X = \sigma_i, b_0$), respectively (For related discussions see, e.g. Refs. \cite{2, 3}). Recent experimental results from CDF \cite{5} at Tevatron, STAR \cite{6} and PHENIX \cite{7} at RHIC and ALICE \cite{8} and LHCb \cite{9} at LHC have demonstrated that the study of coherent interactions in these colliders is feasible and that the data can be used to constrain the description of the hadronic structure at high energies. It motivates the analysis of the production of other final states.

One of the most interesting channels for high energy photon collisions at the LHC is the production of vector mesons such as heavy quarkonia. The exclusive vector meson production in coherent hadron - hadron interactions has been a subject of intense analysis in the last years \cite{10–15}, with a renewed motivation \cite{16–22} associated to the recent experimental data from ALICE and LHCb collaborations. However, it is well known that heavy quarkonia can also be produced in inclusive photoproduction processes, in which the hadron target dissociates, and that the corresponding cross section grows with the energy. The contribution of this process in coherent interactions still is an open question. In this paper we study, for the first time, the inelastic quarkonium production in coherent pp/pPb/PbPb interactions. The main motivation for our analysis is to verify if it is possible to do an experimental study of this channel at LHC in order to elucidate the poorly understood inclusive quarkonium mechanism. Our goal is to obtain an estimate of the total cross sections for $J/\Psi$ and $\Upsilon$ production and the corresponding rapidity distributions for the inelastic production. This process can be considered a background of the exclusive production if we take into account the large event pileup expected at LHC, which difficult the observation of the rapidity gaps in the final states. Consequently, the separation between these two processes should be possible at LHC only if the hadrons in the final states were tagged. Such possibility is currently under study (See e.g. \cite{23}).

A schematic view of the mechanism which we consider in this paper is presented in Fig. 1. Distinctly from the exclusive production, which is characterized by two rapidity gaps in the final state, in the inclusive case we have only one rapidity gap, associated to the photon exchange. Moreover, the photoproduction cross section in the inclusive is linearly proportional to the gluon distribution ($xg$), while in the exclusive case it is proportional to $xg$ squared. The cross section for the inelastic quarkonium photoproduction in a coherent hadron-hadron collision is given by

$$\sigma (h_1 + h_2 \rightarrow h \otimes V + X) = \int \frac{dN}{d\omega} |_{h_1} \sigma_{\gamma h_2 \rightarrow V X} (W_{\gamma h_2}) + \int \frac{dN}{d\omega} |_{h_2} \sigma_{\gamma h_1 \rightarrow V X} (W_{\gamma h_1}) ,$$

where $\otimes$ represents the presence of one rapidity gap in the final state, $\omega$ is the photon energy in the center-of-mass frame (c.m.s.), $\frac{dN}{d\omega} |_{h_i}$ is the equivalent photon flux for the hadron $h_i$, $W_{\gamma h}$ is the c.m.s. photon-hadron energy given...
The study of the production of heavy quarkonium states provides a unique laboratory in which to explore the interplay between perturbative and nonperturbative effects in QCD (For a recent review see, e.g., Ref. [27]). In the last decades, a number of theoretical approaches have been proposed for the calculation of these states, as for instance, the Non Relativistic QCD (NRQCD) approach, the fragmentation approach, the color singlet model (CSM), the color evaporation model and the $k_T$-factorization approach. In the NRQCD formalism [28] the cross section for the production of a heavy quarkonium state $V$ factorizes as $\sigma(ab \to V + X) = \sum_n \sigma(ab \to QQ[n] + X) (O^V[n])$, where the coefficients $\sigma(ab \to QQ[n] + X)$ are perturbatively calculated short distance cross sections for the production of the heavy quark pair $QQ$ in an intermediate Fock state $n$, which does not have to be color neutral. The $\langle O^V[n] \rangle$ are nonperturbative long distance matrix elements (LDME), which describe the transition of the intermediate $QQ$ in the physical state $V$ via soft gluon radiation. Currently, these elements have to be extracted in a global fit to quarkonium data as performed, for instance, in Ref. [29]. In the Color Singlet Model [26], only those states with the same quantum numbers as the resulting quarkonium contribute to the formation of a bound $QQ$ state. This is achieved by radiating a hard gluon in a perturbative process. In contrast, in NRQCD, also color octet $QQ$ states contribute to the
quarkonium production cross section via soft gluon radiation. The Color Singlet Model can be obtained from NRQCD factorization by retaining, for a given process, only the contribution that is associated with the color-singlet LDME of the lowest non-trivial order in $v$, which is the typical velocity of the heavy quark or antiquark in the quarkonium rest frame. It is important to emphasize that the underlying mechanics governing heavy quarkonium production is still subject of intense debate \[27\].

In the specific case of the inelastic $V$ photoproduction, the description of the experimental data for this process is a challenge to the distinct approaches, as verified in Ref. \[30\] and discussed in detail in Refs. \[27, 31\]. In this paper we consider the CSM approach, which predicts that the total cross section can be expressed at leading order as follows (See e.g. \[32\])

$$
\sigma(\gamma + h \rightarrow V + X) = \int dz dp_T^2 \frac{x g_h(x, Q^2) d\sigma}{z(1 - z)}(\gamma + g \rightarrow V + g)
$$

where $z \equiv (p_V . p)/(p_{\gamma} . p)$, with $p_V$, $p$ and $p_{\gamma}$ being the four momentum of the quarkonium, hadron and photon, respectively. In the hadron rest frame, $z$ can be interpreted as the fraction of the photon energy carried away by the quarkonium. Moreover, $p_T$ is the magnitude of the quarkonium three-momentum normal to the beam axis. The partonic differential cross section $d\sigma/dt$ is given by \[32\]

$$
d\sigma/dt(\gamma + g \rightarrow V + g) = \frac{64\pi^2 e_h^2 \alpha_s^2 m_Q}{3} \frac{3}{s^2} \left( s^2 s_1^2 + t^2 t_1^2 + u^2 u_1^2 \right) \langle O^V(3 S_1^{[1]}) \rangle
$$
where $e_Q$ and $m_Q$ are, respectively, the charge and mass of heavy quark constituent of the quarkonium. The Mandelstam variables can be expressed in terms of $z$ and $p_T$ as follows:

\begin{align}
    s &= \frac{p_T^2 + (2m_Q)^2 (1 - z)}{z(1 - z)}, \\
    t &= -\frac{p_T^2 + (2m_Q)^2 (1 - z)}{z}, \\
    u &= -\frac{p_T^2}{1 - z}.
\end{align}

Moreover, $s_1 = s - 4m_Q^2$, $t_1 = t - 4m_Q^2$, $u_1 = u - 4m_Q^2$ and the Bjorken variable $x$ can be expressed by

\begin{align}
    x &= \frac{p_T^2 + (2m_Q)^2 (1 - z)}{W_{\gamma h}^2 z (1 - z)},
\end{align}

where $W_{\gamma h}$ is the photon - hadron center-of-mass energy. The long distance matrix elements (OY($^3S_1^{[1]}$)) can be determined from quarkonium electromagnetic decay rates. In our calculations we use the values as given in Refs. [32] and [33] for the $J/\Psi$ and $\Upsilon$ production, respectively. Moreover, in what follows we consider different parametrizations for the parton distributions. In particular, we use the MRSTLO [34] and CTEQ6L [35] parton distributions for the proton. In the nuclear case, we take into account the nuclear shadowing effects as given by the EPS09 parametrization [36], which is based on a global fit of the current nuclear data.

A comment is in order. In our calculations we will consider the Color Singlet Model at leading order (LO) as given above. As demonstrated in Refs. [37, 38] (See also [39]) the calculation of photoproduction cross section to next-to-leading order (NLO) proved that these corrections are large, increasing towards large transverse momentum of the $J/\Psi$ meson. The corresponding NLO predictions describes the shape of the $z$ and $p_T$ differential $J/\Psi$ cross sections.

![Graph](image-url)

**FIG. 4:** Rapidity distribution for the $J/\Psi$ and $\Upsilon$ production in coherent $pp$ collisions at $\sqrt{s} = 7$ TeV (left panels) and 14 TeV (right panels) considering two different parametrizations for the gluon distribution.

|       | $J/\Psi$ MRSTLO | $J/\Psi$ CTEQ6L | $\Upsilon$ MRSTLO | $\Upsilon$ CTEQ6L |
|-------|------------------|------------------|--------------------|-------------------|
| $\sqrt{s} = 7$ TeV | 17.93 nb (1793 $\times 10^6$) | 13.18 nb (1318 $\times 10^6$) | 0.30 nb (30 $\times 10^6$) | 0.21 nb (21 $\times 10^6$) |
| $\sqrt{s} = 14$ TeV | 25.66 nb (2566 $\times 10^6$) | 18.40 nb (1840 $\times 10^6$) | 0.47 nb (47 $\times 10^6$) | 0.33 nb (33 $\times 10^6$) |

**TABLE I:** The total cross section (event rates) for the inelastic quarkonium photoproduction in coherent $pp$ collisions at LHC energies.
but the normalizations are a factor three below of data \cite{30}, with large uncertainties associated to the choice of the charm quark mass and the factorization and renormalization scales, which indicates that beyond NLO corrections should be included or that contributions of color octet states may be sizeable. In contrast, the total cross section can be described at LO by adjusting the charm quark mass and factorization and renormalization scales and introducing a multiplicative $K$-factor, which takes in account higher-order corrections. It is demonstrated in the Fig. 2 where we compare our predictions, obtained using $Q^2 = p_T^2$, $m_c = 1.5 \text{ GeV}$ and two different parametrizations for the gluon distribution, with the experimental data from H1 Collaboration \cite{30}. We have that, considering distinct values for the $K$-factor, both predictions reasonably describe the data. As the main input for the calculations of the inelastic $J/\Psi$ photoproduction in coherent $pp$ interactions is the energy dependence of the $\gamma + p \rightarrow J/\Psi + X$ cross section, we believe that the use of Color Singlet Model at leading order, with parameters constrained by the HERA data, can be considered a reasonable first approximation for the total cross section and rapidity distribution. Certainly this subject deserves more detailed studies in the future. In what follows we will assume that these same values of $Q^2$ and $K$-factor are valid for $J/\Psi$ production in $pPb$ and $PbPb$ collisions and also for $\Upsilon$ production with $m_b = 4.5 \text{ GeV}$.

III. RESULTS

Let’s calculate the rapidity distribution and total cross section for the inelastic quarkonium photoproduction in coherent $pp$, $pPb$ and $PbPb$ collisions. The distribution on rapidity $Y$ of the quarkonium in the final state can be directly computed from Eq. (1), by using its relation with the photon energy $\omega$, i.e. $Y \propto \ln (\omega/\mathcal{M}_V)$. Explicitly, the rapidity distribution is written down as,

$$
\frac{d\sigma}{dY} [h_1 + h_2 \rightarrow h \otimes V + X] = \left[ \frac{dN}{d\omega} [h_1 \sigma_{\gamma h_2 \rightarrow V X} (\omega)] \right]_{\omega_L} + \left[ \frac{dN}{d\omega} [h_2 \sigma_{\gamma h_1 \rightarrow V X} (\omega)] \right]_{\omega_R}
$$

where $\otimes$ represents the presence of a rapidity gap in the final state and $\omega_L (\propto e^{-Y})$ and $\omega_R (\propto e^{Y})$ denote photons from the $h_1$ and $h_2$ hadrons, respectively. As the photon fluxes, Eqs. (2) and (3), have support at small values of $\omega$, decreasing exponentially at large $\omega$, the first term on the right-hand side of the Eq. (8) peaks at positive rapidities while the second term peaks at negative rapidities. Consequently, given the photon flux, the study of the rapidity distribution can be used to constrain the photoproduction cross section for a given energy. Moreover, in contrast to the total rapidity distributions for $pp$ and $PbPb$ collisions, which will be symmetric about midrapidity ($Y = 0$), $d\sigma/dY$ will be asymmetric in $pPb$ collisions due to the differences between the fluxes and process cross sections.

Following Ref. \cite{30} we will integrate the fraction of the photon energy carried away by the quarkonium in the range $0.3 \leq z \leq 0.9$. Our predictions do not include resolved photoproduction, which contributes appreciably only at $z \lesssim 0.3$ and diffractive production, which is confined to the quasielastic domain at $z \approx 1$ and $p_T \approx 0$. These contributions are in general excluded from experimental measurements (See Ref. \cite{30} and Fig. 2) in order to make a meaningful comparison. In order to estimate the dependence of our results on the inferior limit of integration $z_{\text{min}}$, in Fig. 3 we present our predictions for the rapidity distribution for $J/\Psi$ production in coherent $pp$ collisions at $\sqrt{s} = 14 \text{ TeV}$ obtained using the CTEQ6L parametrization and different values of $z_{\text{min}}$. We have that our predictions increase by $\approx 23\%$ at midrapidity if we assume $z_{\text{min}} = 0$. Similar behaviour is observed for other energies and for $\Upsilon$ production.

FIG. 5: (Color online). Rapidity distribution for the inelastic $J/\Psi$ photoproduction in coherent $PbPb$ collisions at $\sqrt{s} = 5.5 \text{ TeV}$ disregarding (left panel) and taken into account (right panel) the nuclear shadowing corrections. See text.
TABLE II: The total cross section (event rates) for the inelastic quarkonium photoproduction in coherent $PbPb$ collisions at $\sqrt{s} = 5.5$ TeV.

|         | CTEQ       | CTEQ + EPS09 |
|---------|------------|--------------|
| $J/\Psi$ | 6122.0 $\mu$b ($2571 \times 10^4$) | 4647.6 $\mu$b ($1951 \times 10^4$) |
| $\Upsilon$ | 71.9 $\mu$b ($30 \times 10^3$) | 60.6 $\mu$b ($25 \times 10^3$) |

FIG. 6: (Color online). Rapidity distribution for the inelastic $J/\Psi$ photoproduction in coherent $pPb$ collisions at $\sqrt{s} = 5.5$ TeV. The $\gamma p$ and $\gamma Pb$ contributions are explicitly presented in the left panel. In the right panel we present the predictions obtained disregarding and taken into account the nuclear shadowing corrections.

In Fig. 4 we present our predictions for the inelastic $J/\Psi$ and $\Upsilon$ photoproduction in coherent $pp$ collisions at LHC energies. As expected, the total rapidity distributions are symmetric about the midrapidity. We calculate $d\sigma/dY$ considering different parametrizations for the gluon distribution in the proton. It is important to emphasize that the rapidity distribution at LHC probes a large interval of photon-proton center of mass energy since $W_{A}^{2} \approx M_{V} \sqrt{s} \exp(\pm Y)$, which corresponds to very small $x \approx M_{V} e^{-|Y|}/\sqrt{s}$. The MRSTLO and CTEQ6L predictions differ by $\approx 30\%$ at $Y = 0$, with the CTEQ6L one being a lower bound. In Table I we present our estimates for the total cross sections and production rates assuming the design luminosity $L_{\text{LHC}} = 10^{7}$ mb$^{-1}$s$^{-1}$ and a run time of $10^{7}$ seconds. We predict large values for the events rate and cross sections of the order of units of nb, in contrast with values of the order of $100 \mu$b for the inclusive quarkonium hadroproduction $^{27}$. Despite their much smaller cross sections, the clean topology of coherent processes implies a larger signal to background ratio. Therefore, the experimental detection is in principle feasible. However, as already emphasized in the Section III the signal is expected to be reduced due to the event pileup and an alternative to measure coherent events at the LHC is by tagging the intact hadron in the final state.

In what follows we will consider coherent $PbPb$ and $pPb$ collisions. We will assume that the gluon distribution in the proton, $x_{g_{p}}$, is given by the CTEQ6L parametrizations and that the nuclear gluon distribution is given by $x_{g_{A}} = A R_{g} x_{g_{p}}$, where $R_{g}$ takes into account nuclear shadowing effects as given by the EPS09 parametrization $^{36}$. In Fig. 5 we present our predictions for the inelastic $J/\Psi$ photoproduction in coherent $PbPb$ collisions at $\sqrt{s} = 5.5$ TeV. In the left panel we present the predictions obtained disregarding the shadowing corrections ($R_{g} = 1$), while in right panel these corrections are taken into account. The two contributions of Eq. (8) are presented separately as well as the sum (solid line). As in the $pp$ case, the total rapidity distributions are symmetric about the midrapidity. However, we observe larger values for the rapidity distribution due to the enhancement of the photon flux for a nucleus, which is proportional to $Z^{2}$. As for the LHC energies the typical values of $x$ are $\approx M_{V} e^{-|Y|}/\sqrt{s}$, we are probing the shadowing corrections ($R_{g} < 1$) in the nuclear gluon distributions. As we can see in Fig. 5 the behaviour of the rapidity distribution is strongly modified by these corrections. In Table II we present our estimates for the total cross sections and event rates assuming the design luminosity $L_{\text{LHC}} = 0.42$ mb$^{-1}$s$^{-1}$.

Let's discuss now the inelastic $J/\Psi$ photoproduction in coherent $pPb$ collisions, considering that $h_{1} = p$ and $h_{2} = Pb$. As discussed before, in this case we expect asymmetric rapidity distributions, with the contribution of the $\gamma p$ and $\gamma Pb$ interactions being different. In $\gamma p$ interactions the photon comes from the nuclei, with the photon flux being proportional to $Z^{2}$, and the photoproduction cross section being determined by the gluon distribution of the proton ($x_{g_{p}}$). In $\gamma Pb$ interactions the photon comes from the proton and the photoproduction cross section being determined...
by the gluon distribution of the nuclei, which is enhanced by a factor of the order of $x_g$.

In Fig. 6 (left panel) we explicitly show the different contributions for the rapidity distribution for $\sqrt{s} = 5.5$ TeV disregarding nuclear shadowing effects. As expected, the $\gamma p$ contribution peaks for negative rapidities and $\gamma Pb$ one for positive rapidities, with the rapidity distribution being asymmetric. In Fig. 6 (right panel) we present our predictions considering the nuclear shadowing effects, which are small, since the rapidity distributions is dominated by $\gamma p$ interactions. In Table III we present our estimates for the total cross sections and production rates assuming the design luminosity $L_{\text{pPb}} = 150 \text{ mb}^{-1}\text{s}^{-1}$ and a run time of $10^6$ seconds. We predict cross sections that are two orders of magnitude smaller than those obtained in the $PbPb$ case. The larger $pA$ luminosity, which is two order of magnitude higher than for $AA$, counteracts this suppression for the event rates. However, the resulting events rates still are small in comparison to the $pp$ results. Recently, an upgraded $pPb$ scenario was proposed in Ref. [40], which improve the $pPb$ luminosity and the running time. These authors proposed the following scenario for $pPb$ collisions: $L_{\text{pPb}} = 10^4 \text{ mb}^{-1}\text{s}^{-1}$ and a run time of $10^7$ s. The corresponding event rates also are presented in the Table III. In this case we have numbers similar to those for $pp$ collisions, which makes the experimental analysis feasible. Another advantage of $pPb$ collisions is that it is expected to trigger on and carry out the measurement with almost no pileup [40]. Therefore, the upgraded $pA$ scenario provides one of the best possibilities to detect the inelastic $J/\Psi$ photoproduction in coherent processes.

Our predictions for the inelastic $\Upsilon$ photoproduction in coherent $pPb$ and $PbPb$ collisions are presented in Fig. 7. In comparison to the $J/\Psi$ case, the predictions are reduced by two orders of magnitude, which is directly associated to the larger mass of the $\Upsilon$. Moreover, the rapidity distribution is also reduced at midrapidity by the nuclear shadowing effects. The corresponding values for the cross sections and event rates are presented in the Tables II and III.

Finally, let's compare our predictions with those obtained in Ref. [14] for the exclusive quarkonium production. Although in [14] the numbers were obtained considering the color dipole formalism and taking into account saturation effects, similar predictions has been obtained using other approaches [10, 12, 13, 17, 18]. Our predictions for the inclusive quarkonium photoproduction in $pp/pPb/PbPb$ collisions are a factor $\gtrsim 4$ smaller than the exclusive $J/\Psi$ production. In the $\Upsilon$ case, the inclusive production is a factor $\gtrsim 3$ smaller than the exclusive one. It is important to emphasize that distinctly from the $J/\Psi$ case, which have its parameters constrained by the $ep$ HERA data, the predictions for the $\Upsilon$ production were obtained considering an educated guess for the parameters. This may be an explanation for the different values for the reduction factors for $J/\Psi$ and $\Upsilon$ production. Our results demonstrate that the contribution of the inelastic channel for quarkonium photoproduction is non-negligible. Moreover, if the experimental separation of the inelastic quarkonium photoproduction in coherent interactions were possible, the large numbers obtained in our calculations indicate that this process could be used to study the underlying mechanism.
governing heavy quarkonium production.

IV. CONCLUSIONS

In this paper we have computed for the first time the cross sections for the inelastic quarkonium photoproduction in coherent \( pp/pPb/PbPb \) collisions at LHC energies. We predict sizeable values for the cross sections and event rates. In comparison with the exclusive production, the inelastic channel is non-negligible, being smaller by a factor \( > 3 \). The experimental separation between the exclusive and inclusive quarkonium photoproduction still is an open question, in particular considering the large pileup event expected to occur at LHC. However, if the separation were possible, using for example forward detectors for the tagging of the hadrons in the final state, the inelastic quarkonium photoproduction in coherent interactions could be used to improve our understanding of the mechanism of quarkonium production. Certainly our analysis deserves more detailed studies in several aspects, as for example the inclusion of next-to-leading order corrections to the Color Singlet Model, the study of differential distributions and the calculation of the quarkonium photoproduction using the NRQCD formalism. We plan to do these studies in forthcoming publications.

Acknowledgments

This work was supported by CNPq, CAPES and FAPERGS, Brazil.

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