Interfacing scalable photonic platforms: solid-state based multi-photon interference in a reconfigurable glass chip

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Scaling-up optical quantum technologies requires to combine highly efficient multi-photon sources and integrated waveguide components. Here, we interface these scalable platforms: a quantum dot based multi-photon source and a reconfigurable photonic chip on glass are combined to demonstrate high-rate three-photon interference. The temporal train of single-photons obtained from a quantum emitter is actively demultiplexed to generate a 3.8 kHz three-photon source, which is then sent to the input of a tuneable tritter circuit, demonstrating the on-chip quantum interference of three indistinguishable single-photons. Pseudo number-resolving photon detection characterising the output probability distribution shows that this first combination of scalable sources and reconfigurable photonic circuits compares favourably in performance with respect to previous implementations. A detailed cost-budget shows that merging solid-state based multi-photon sources and reconfigurable photonic chips could allow ten-photon experiments on chip at ~40 Hz rate in a foreseeable future.

INTRODUCTION

The development of optical quantum technologies allows for quantum-enhanced metrology, secure quantum communication, and quantum computing and simulation in highly-increased dimensions. Maturing quantum photonics requires efficient generation and detection of single-photons, as well as their scalable manipulation.1 Single-photon detection is a well-advanced technology to date, and has already reached near-optimal values in efficiencies. Recent advances in single-photon generation, significant advances have been demonstrated using heralded approaches based on frequency conversion,6,7; however, their single-photon purity unavoidably decreases with the source brightness, which is defined as the probability of providing a single-photon per excitation pulse. Temporal multiplexing schemes have been explored to circumvent this limitation, but at the expense of overall operation rates. On the other hand, spatial multiplexing schemes of many heralded sources implies a dramatic increase of resource overhead.

Recently, scalable technologies for single-photon generation have emerged using quantum dots (QDs) in microcavities,8,11,14, where a single artificial atom emits temporal trains of single photons on demand. The brightness already exceeds by more than one order of magnitude that of heralded sources of the same quality and near-deterministic sources could be reached with a similar technology and modified excitation scheme. This new generation of sources has allowed multiphoton experiments such as Boson Sampling involving up to five detected single-photons.

Photon manipulation can suffer from mechanical instabilities in bulk circuits, which lead to optical phase drifts and induces errors in device performance. A scalable photonic platform should instead provide photon routing and control in low-loss, integrated, and reconfigurable chips. These devices have been developed using various materials, such as silicon, silicon nitride, lithium niobate, or glass; the latter, based on femtosecond laser writing, offers fast and cheap production, and has been used to tackle a variety of complex quantum operations, such as Boson Sampling, quantum Fourier transforms, and quantum walks. In addition, this technique has shown great versatility in terms of polarization control and 3D patterning; thermally tuneable phase-shifters can also be conveniently integrated to achieve circuit reconfigurability. Despite spectacular progress on both solid-state photon sources, and reconfigurable photonic circuits on chip, these two promising platforms have not yet been combined—an approach that can result crucial for scaling optical quantum technologies.

In this work, we interconnect both scalable photonic platforms: we observe three-photon coalescence using an efficient solid-state based multi-photon source, and a reconfigurable photonic tritter circuit on glass. This first implementation of joint platforms already shows an improved performance in terms of quantity and quality of the three-photon interference. Furthermore, we estimate...
that feasible improvements can allow for ten-photon experiments at ~40 Hz rates in the near future.

The experimental scheme, sketched in Fig. 1, is composed by four modules: (I) single-photon generation at high rates from a QD source, (II) time-to-spatial active demultiplexing to prepare a three-photon source, (III) photonic circuit of the reconfigurable tritter, and (IV) detection of the photonic state via pseudo number-resolving measurements. In the following, we present each module before discussing the performances of the combined system.

**SINGLE-PHOTON SOURCE**

We use a solid-state single-photon source consisting of a single InGaAs/GaAs QD deterministically coupled, with nanometric accuracy, to a micropillar cavity [30]. The micropillar device is gradually doped in the vertical direction to form a p-i-n diode structure embedding the QD in the intrinsic region of the cavity. Electrical contacts are defined in the top and bottom parts of the pillar to gain tunability of the QD energy via the confined Stark effect [11, 37]. The device is mounted in a closed-cycle cryostat at ~8 K, and an optical confocal cross-polarisation setup is used to excite the single-photon source with a resonant pulsed laser, see Fig. 1(I).

The experiments are performed with a neutral exciton in resonance with the cavity mode, which presents a single-photon lifetime of 160 ps and a wavelength of 925.47 nm. This short single-photon lifetime allows increasing the laser repetition rate (81 MHz) by a factor of 4 using a passive pulse multiplier composed of BSs and delay lines [38].

The first lens brightness of the source is measured to be $p_1=16.0\%$ in line with state of the art performances for neutral exciton [8]. The fibered brightness is measured to be $p_2=7.0\%$, where this value is limited by a finite numerical aperture N.A.=0.45 of the first lens. This corresponds to a generation rate of 22 MHz of single-photons in a single-mode fiber for a 324 MHz pumping rate. Standard photon correlation measurements are used to characterise the source performance under a repetition rate of 81 MHz. The single-photon purity is found to be $g^{(2)}(0)=0.035\pm0.003$, and the photon indistinguishability corrected (uncorrected) from $g^{(2)}(0)$ is measured to be $M=0.920\pm0.007$ (0.850$\pm0.007$) for ~12.5 ns between emitted photons, and 0.880$\pm0.009$ (0.810$\pm0.009$) for ~100 ns maximum temporal distance between the emitted photons subsequently used for interference.

**DEMULTIPLEXER**

Multi-photon interference requires the efficient preparation of indistinguishable single-photons arriving simultaneously to the input ports of a photonic circuit [16, 17, 39]. One can build the required multi-photon sources starting from a single-photon source via a demultiplexer: a device that routes its input train of temporal modes into separate and simultaneous spatial modes. In general, a demultiplexer can be characterised by their relative time-varying output signals. The device is a passive demultiplexer if these signals are static in time, and its conversion rate—the ratio between the output $n$-photon event rates, and the input single-photon rate—is given by

$$C_n^{(\text{passive})} = \prod_{k=1}^{n} p_k^{\text{out}},$$

where $p_k^{\text{out}}$ is the static probability of the input signal to exit the $k$–th output. For instance, in the particular case with $n$ equal output probabilities $p_k^{\text{out}}=1/n$, the conversion rate scales as $C_n^{(\text{passive})}=(1/n)^n$, showing the non scalability of passive approaches. On the other hand, an active demultiplexer with time-varying relative output signals $S^{\text{out}}(t)$ results in a conversion rate $C_n^{(\text{active})} = \int_T \left[ \prod_{k=1}^{n} S_k^{\text{out}}(t) \right] dt$, where the integral is taken over the demultiplexing period $T$. In this active case, the conversion rate is typically polynomial in $n$, thus constituting a scalable approach.

Solid-state based demultiplexed multi-photon sources have been reported with both passive [14] and active schemes [16, 17, 40]. Thus far, approaches for active demultiplexing have employed either on-chip architectures [40] with fast reconfigurable speeds (20 MHz), but low device throughput transmission; or have combined high-transmission bulk electro-optic modulators (pockels cells) [16, 17], but requiring very high volt-
ages (~2000 V) for each modulator, and with relatively slow reconfigurable speeds (0.76 MHz). Here we make use of resonance-enhanced electro-optical modulators (r-EOMs), QUBIG GmbH, that allow for combining high transmission and fast reconfigurability, while requiring low-voltage control (~5 V).

Figure 2(I) depicts our demultiplexing scheme for preparing a 3-photon source. The system consists of two cascaded high-transmission (95%) and synchronised r-EOMs. The first r-EOM is driven at one eighth of the laser rep. rate, ~10 MHz, which combined with a polarising beam-splitter (PBS) distributes 50 ns long time-bins to either output of the PBS alternately. Similarly, a second r-EOM, driven at one sixteenth of the laser rep. rate, ~5 MHz, now routes 100 ns long time-bins to either output of the second PBS. Fibered delays of appropriate length are added here to ensure the simultaneous arrival of the three single-photons to the tritter circuit.

Figure 2(b) shows our measured output signals for the same demultiplexing period of T=200 ns, taken using laser light and photodiodes. The non-unity contrast of modulation is due to both imperfect polarisation switching of the r-EOMs, and finite polarisation extinction ratios of the PBSs. Using the same demultiplexing scheme with the single-photon source operated at the increased pump repetition rate of 324 MHz, we obtain detected, and generated—corrected for detector efficiencies of 0.3—2 and 3-photon rates as shown in Fig. 3 for both active and passive schemes. The generated (detected) 3-photon production rates between active and passive schemes, and can be used to assess the demultiplexer’s active efficiency \( \eta_a = (r_n^{(exp)} - 1)/(r_n^{(ideal)} - 1) \)—a quantity that equals 1 for an ideal active scheme, and vanishes for a passive one.

Given the modulation sequences, we can estimate the 3-photon conversion rates \( C_3 \) for both the ideal active, and passive scenarios. For the ideal active case, we obtain \( r_3^{(active)} = 1/4 \); that is, the time-integrated area of the product of all three relative output signals is one fourth of the total demultiplexing area (period) of \( T=200 \text{ ns} \). If the demultiplexer is turned off, thus operated as a passive one, the conversion rate now becomes \( C_3^{(passive)} = 1/32 \)—the product of three static transmission probabilities 1/4, 1/4, and 1/2. The active-to-passive ratio \( r_n = C_n^{(active)}/C_n^{(passive)} \) relates the relative \( n \)-photon production rates between active and passive schemes, and Figure 2(b) shows our measured output signals for the same demultiplexing period of \( T=200 \text{ ns} \), taken using laser light and photodiodes. The non-unity contrast of modulation is due to both imperfect polarisation switching of the r-EOMs, and finite polarisation extinction ratios of the PBSs. Using the same demultiplexing scheme with the single-photon source operated at the increased pump repetition rate of 324 MHz, we obtain detected, and generated—corrected for detector efficiencies of 0.3—2 and 3-photon rates as shown in Fig. 3 for both active and passive schemes. The generated (detected) 3-photon production rates between active and passive schemes, and can be used to assess the demultiplexer’s active efficiency \( \eta_a = (r_n^{(exp)} - 1)/(r_n^{(ideal)} - 1) \)—a quantity that equals 1 for an ideal active scheme, and vanishes for a passive one.

Figure 2(I) illustrates the working principle of the demultiplexer. The synchronised operation of both r-EOMs results in the active distribution of consecutive ~50 ns long time bins into different spatial outputs, see Fig. 2(a).

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The output of the demultiplexer is connected to a fiber array precisely coupled to the tritter chip inputs. The optical waveguides are fabricated by femtosecond laser writing in a commercial alumino-borosilicate glass substrate (EagleXG, Corning Inc., USA). A Yb:KYW cavity-dumped mode-locked laser oscillator was employed, producing 300 fs duration pulses at 1 MHz repetition rate. In detail, 220 nJ laser pulses were focused 30 µm below the surface of the glass substrate, by means of a 0.6 N.A. microscope objective, while the sample was translated at the constant speed of 20 mm/s. Such irradiation parameters result in single-mode waveguides at 930 nm wavelength with ~8 µm 1/e² mode-diameter and < 1 dB/cm propagation loss.

As shown in Fig. 1 the tritter is built of three directional couplers (DCs), with nominal reflectivities of \( R_1 = 1/2 \) (first and last DCs), and \( R_2 = 1/3 \) (second DC), and one intermediate phase-shifter \( \phi \). When the phase shifter is set at \( \phi = \pi/2 \) or \( 3\pi/2 \), the theoretical unitary matrix of the circuit corresponds to a symmetric tritter transformation \([41][44]\), given by the matrix elements \( U_{jk} = \exp[i2\pi(j-1)(k-1)]/\sqrt{3} \), where \( j,k = 1,2,3 \) are the corresponding matrix elements indexes. At the input and at the output of the chip the inter-waveguide distance is set to 127 µm to match the pitch of the fiber arrays. The overall footprint of the waveguide circuit is \( 25 \times 0.25 \) mm².

The tuneable phase-shifter \( \phi \) is realized according to the method of Refs. [34][35]. A 50 nm-thick gold layer is sputtered on the top surface of the chip, and a resistive heater is laser-patterned just above the relevant waveguide (the obtained resistance value is about 60 Ω). By driving the resistor with a suitable voltage, the waveguide is locally heated and increases its refractive index according to the thermo-optic effect, thus producing a finely adjustable phase delay.

We characterize the experimental matrix \( U^{\text{exp}} \) using a continuous-wave laser tuned to the same wavelength as that of the single-photons. We exploit the method described in Ref. [55] where amplitudes and phases are deduced by measuring the intensity and by monitoring the interferences at the chip outputs when sending the laser directly into one input only or into two inputs simultaneously. For an applied voltage of 3.1 V on the phase shifter, providing the best operation, we obtain a fidelity \( F = 0.960 \), the visibility \( V \) is given by the ratio \( V = \frac{|\langle \phi | \hat{\mathcal{U}} | \psi \rangle|}{\langle \phi | \hat{\mathcal{U}} | \phi \rangle} \). Each output is coupled to two cascaded fibered BSs connected to three silicon APDs. An electronic correlation allows one to reconstruct all the triple photon coincidences. We accumulated a total of 3078 detected triple events during ~1.7 hours, collected within a 2 ns coincidence window. The corresponding reconstruction of the output state is shown in Fig. 4(b) in blue bars. There is a strong contribution of the three-photon bunching terms and the non-collision term with an average probability of \( P_{|3,0,0\rangle} = 0.157 \pm 0.015 \) and \( P_{|1,1,1\rangle} = 0.229 \pm 0.011 \), respectively, and an average probability for the terms associated to distinguishable photons \( P_{|2,1,0\rangle} = 0.050 \pm 0.006 \).

To compare our experimental results with the theoretical distribution calculated for the measured mean wave-packet overlap and the non-zero \( g^{(2)}(0) \). The effect of non-perfect indistinguishability is accounted for following the model of generalised multiphoton interference by Tillmann and coworkers [46]. However, such model does not consider the generation of more than one photon per pulse. To do so, one needs to identify the origin of non perfect \( g^{(2)}(0) \), since different contributions are expected whether the extra photons are identical to the others or not. Here, we use a neutral exciton under the mirror, with a different contribution, as a reference state. The effect of this model is described for the tritter circuit.
tive amount of average photon number coming from the QD emission, \( \mu_{QD} = p_L^{QD} \), and from the scattered laser, \( \mu_L \), according to the formalism of the probability generating function \( \chi \) (see supplementary material). The second order autocorrelation function that results from the mixture of the independent photonic distributions of scattered laser and QD single-photons is given by \( g^{(2)}(0) = \chi(2 + \chi)/(1 + \chi)^2 \), where \( \chi = \mu_L/\mu_{QD} \). Since we measure a high single-photon purity, we approximate the probability of having a single-photon from the laser by \( p_L^{(2)}(0) \propto g^{(2)}(0) p_{QD}^{2} \), neglecting higher order Fock terms from the laser \( p_{L}^{(k+1)} \ll p_{L}^{(1)} \).

Following this assumption, we consider that for each input mode there is a certain probability of having vacuum, a single-photon from the QD, a single-photon from the laser, or most unlikely simultaneous photons from QD and laser. The total sum of these probabilities is normalised such that \( p_0 + p^{QD}_1 + p^{L}_1 + p^{QD,L}_1 = 1 \). In this context and considering that \( p_{QD} \gg p_L^{QD} \), the relevant input tritter states involving three photons are: \( |1_{QD},1_{QD},1_{QD} \rangle \) with probability \( (p_L^{QD})^3 \), the six combinations of \( \{|1_{QD}1_L,1_{QD},0\rangle\} \) with probability \( p_0(p_L^{QD})^2 p_L^1 \), and the three combinations of \( \{|1_{QD},1_{QD},1_L\rangle\} \) with probability \( (p_L^{QD})^2 p_L^1 \). The total output distribution is obtained by summing the weighted contributions of all relevant input states and considering the corresponding pair-wise indistinguishabilities between photons generated from the QD, and \( M=0 \) between QD single-photons and laser light.

Our source single-photon purity is measured to be \( g^{(2)}(0) = 0.035 \pm 0.003 \). However, when running our experiments with a laser repetition rate of 324 MHz, we observe a slightly deteriorated effective single-photon purity of \( g^{(2)}(0) = 0.071 \pm 0.003 \), due to the slow jitter time of our detectors, which we take into account in our modelling, see Supplementary Material. Figure 4b) shows our experimental results, displaying a good agreement between our measurements and simulations.

### DISCUSSION & CONCLUSION

Table I shows various figures-of-merit of sources used in implementations of three-photon interference in a tritter device. Previous experiments used an integrated platform for either the source, or the photonic circuit, but not both simultaneously. The present implementation is the first combining both integrated platforms, already showing a significant improvement in performance.

The brightness of the QD single-photon source, combined with an active demultiplexer provides an increase by at least two orders-of-magnitude of the three-photon generation rate. Moreover, also the tritter output three-photon rate is increased by a factor of \(~2\) and its distribution is closer to the ideal one compared to previous works, see Fig. 4c. These significant advances have been obtained despite non-minimised losses in the present implementation (see Table II), and using low-efficiency detectors with limited time resolution. The present study thus constitutes a first step on improving the scalability that can be obtained by merging solid-state photon sources and reconfigurable chips.

Given the challenges imposed in this first merging of scalable photonic platforms, where not all parts of the
system could be optimised at once, we present in Table II a loss-budget indicating values within reach in the foreseeable future. On the source side, the first lens brightness was limited by the use of a resonant excitation scheme that removes more than 50% of the single-photons. Recent studies show that such excitation scheme could be overcome using side excitation [48] or simply removed by taking advantage of Raman assisted excitation [49]. We thus anticipate that the first lens brightness using this new excitation scheme could reach the maximal value resulting from the Purcell acceleration and outcoupling efficiency, typically 65% for the present technology [11]. The fibered brightness was limited here to 7% due to the use of a microscope objective with relatively small numerical aperture within our collection setup (N.A.=0.45). Inserting a high numerical aperture collection lens inside the cryostat has been shown to solve this problem [10]. Moreover, recent technological progress on the glass chip technology shows that its throughput transmission could reach much higher values, by adopting proper post-processing with thermal-annealing after the waveguide inscription [50]. Considering all these possible improvements, we anticipate that one could soon reach on-chip ten-photon manipulation at rates as high as ~40 Hz.

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TABLE II. Efficiency budget for the total architecture and foreseen progress in the near future (see details in the text).

| Parameter | This work | Optimised values |
|-----------|-----------|------------------|
| Repetition rate (MHz) | 324 | 1000 |
| First lens brightness | 0.16 | 0.65 |
| Fibered brightness | 0.07 | 0.50 |
| Demultiplexer transmission (per photon) | 0.63 | 0.85 |
| Chip transmission + fiber-array coupling per photon | 0.17 | 0.60 |
| Detection efficiency per photon | 0.30 | 0.9 |
| Gen. (Det.) 3-photon rate source (Hz) | 3.8×10^4 (105) | 16×10^6 (12×10^6) |
| Gen. (Det.) 3-photon rate after chip (Hz) | 19 (0.5) | 5.5×10^6 (4.0×10^6) |
| Output det. 10-photon rate (Hz) | - | 40 |

The rates as high as one could soon reach on-chip ten-photon manipulation at all these possible improvements, we anticipate that annealing after the waveguide inscription [50]. Considering all these possible improvements, we anticipate that the first lens brightness using this new excitation scheme could be overcome using side excitation [48] or simply removed by taking advantage of Raman assisted excitation [49]. We thus anticipate that the first lens brightness using this new excitation scheme could reach the maximal value resulting from the Purcell acceleration and outcoupling efficiency, typically 65% for the present technology [11]. The fibered brightness was limited here to 7% due to the use of a microscope objective with relatively small numerical aperture within our collection setup (N.A.=0.45). Inserting a high numerical aperture collection lens inside the cryostat has been shown to solve this problem [10]. Moreover, recent technological progress on the glass chip technology shows that its throughput transmission could reach much higher values, by adopting proper post-processing with thermal-annealing after the waveguide inscription [50]. Considering all these possible improvements, we anticipate that one could soon reach on-chip ten-photon manipulation at rates as high as ~40 Hz.

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