Strategic Cell-Cycle Regulatory Features That Provide Mammalian Cells with Tunable G1 Length and Reversible G1 Arrest

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Abstract

Transitions between consecutive phases of the eukaryotic cell cycle are driven by the catalytic activity of selected sets of cyclin-dependent kinases (Cdks). Yet, their occurrence and precise timing is tightly scheduled by a variety of means including Cdk association with inhibitory/adaptor proteins (CKIs). Here we focus on the regulation of G1-phase duration by the end of which cells of multicelled organisms must decide whether to enter S phase or halt, and eventually then, differentiate, senesce or die to obey the homeostatic rules of their host. In mammalian cells, entry in and progression through G1 phase involve sequential phosphorylation and inactivation of the retinoblastoma Rb proteins, first, by cyclin D-Cdk4,6 with the help of CKIs of the Cip/Kip family and, next, by the cyclin E-Cdk2 complexes that are negatively regulated by Cip/Kip proteins. Using a dynamical modeling approach, we show that the very way how the Rb and Cip/Kip regulatory modules interact differentially with cyclin D-Cdk4,6 and cyclin E-Cdk2 provides to mammalian cells a powerful means to achieve an exquisitely-sensitive control of G1-phase duration and fully reversible G1 arrests. Consistently, corruption of either one of these two modules precludes G1 phase elongation and is able to convert G1 arrests from reversible to irreversible. This study unveils fundamental design principles of mammalian G1-phase regulation that are likely to confer to mammalian cells the ability to faithfully control the occurrence and timing of their division process in various conditions.

Introduction

Living systems are born to reproduce and the most important challenge individual cells are faced with in their life is to decide whether and when it is time to divide. This decision is usually made during G1 phase (the lag phase that separates mitosis from the initiation of DNA replication) of the cell-division cycle, shortly before S-phase entry, at a specific ‘Start’ point in budding yeast [1], called restriction (R) point in animal cells [2], beyond which cells are irrevocably committed to divide independently of exogenous cues. While S-phase entry relies on the abrupt accumulation of active cyclin E-Cdk2 complexes in the nucleus, eukaryotic cells have evolved two major mechanisms to delay and prevent G1/S transit [3]: (i) downregulation of cyclin synthesis; (ii) inhibition of the cyclin E-Cdk2 activity by association with Cdk inhibitory proteins (CKIs). The first mechanism, which primarily affects local and systemic controls restrain cell division in order to maintain tissue homeostasis and prevent the emergence of cancer [9,10]. There is clear evidence that interaction between the two G1-specific activatory modules, cyclin D-Cdk4,6 and cyclin E-Cdk2, and CKIs plays a paramount role in mammalian G1-phase control. It is still obscure, however, what particular features of this interaction might enable mammalian cells to precisely control in a contextual manner the length of their G1 phase [11,12] and, ultimately, make the right decision regarding the occurrence of one amongst its many possible outcomes, i.e. cell division, differentiation, senescence or death [13]. The mammalian G1 regulatory network presents two striking designs that, conceivably, could participate in these events. First, cyclin D-Cdk4,6 and cyclin E-Cdk2 are activated sequentially during G1-phase progression owing to the fact that cyclin E transcription is repressed by unphosphorylated Rb proteins via the mobilization of chromatin-modifying factors and is relieved following partial Rb phosphorylation by cyclin D-Cdk4,6 [14,15]. Second, CKIs of the Cip/Kip family that accumulate in response to stress or differentiation signals exert an opposite effect on cyclin D-Cdk4,6 and cyclin E-Cdk2 as they facilitate the activity of the former complexes while they inhibit the activity of the latter ones [16–18]. In multicellular organisms like mammals, cell division actively takes place during development and tissue regeneration. This is no longer true, however, in most fully-developed organs in which local and systemic controls restrain cell division in order to keep tissue homeostasis and prevent the emergence of cancer [9,10].

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Figure 1. CKI-dependent regulation of mammalian G1-phase progression. (A) Cells leaving G0 following growth-factor stimulation \( (I_{GF}) \) and exposed to stress/differentiation signals \( (I_{SF}) \) during G1 phase may be driven towards either one of two alternative fates: either G1-phase elongation or G1-arrest, which can be reversible or irreversible. (B) G1-phase progression in the presence of both \( I_{GF} \) and \( I_{SF} \) signals relies on a tight competition between two major players: \( I_{GF} \)-induced cell-cycle activators and \( I_{GF} \)-induced cell-cycle inhibitors. Main positive regulators (grey ellipses) are the G1-specific, D- and E-type cyclins together with their favorite CDK partners and one subfamily of transcriptional factors termed activator E2Fs, which ultimately trigger S-phase entry. Negative regulators (white ellipses) include the unphosphorylated and hypophosphorylated Rb proteins and the members of the Cip/Kip family of CKIs (p21Cip1, p27Kip1, p57Kip2). Note that cyclin D-Cdks and cyclin E-Cdks are differentially regulated by unphosphorylated Rb and Cip/Kip proteins (see asterisks).

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thus addressed the following questions: How does the singular organization of the mammalian G1 regulatory network determine the rate of G1-phase progression and shape the properties of G1 arrest? More generally, are there specific decision-making strategies encoded at the level of this sophisticated molecular network organization?

To answer these issues, we used a modeling approach that has proved useful to unveil design principles of molecular networks, especially those involved in cell-cycle regulation [19]. Yet, because our interest was more specifically focusing on the G1-phase period, a model of the whole cell cycle was not necessarily of use [20,21]. That is why, we built and analysed a molecular network model limited to the cell-cycle period going from G0 exit to S-phase entry [22–26]. A major improvement of our model on previous ones in the field lies in the fact that it incorporates some detailed features of the interaction between the G1-specific cyclin-Cdks and the Rb/E2F and Cip/Kip regulatory modules. The model does not only reproduce the typical, previously-described properties of G1/ S transition, including discreetness and irreversibility, but it also reveals how stockpiling of the Cip/Kip proteins in response to stress signals impinges on G1-phase progression such as to endow mammalian cells with the ability to easily adjust the length of their G1 phase and sustain a reversible G1 arrest. Consistently, we found that reducing the selectivity of inhibitory controls over cyclin D-Cdk4,6 and cyclin E-Cdk2 precludes long-lasting G1 phases and converts the reversible G1 arrest into irreversible ones. We further stress that these poles apart types of cell-cycle arrest correspond to two qualitatively distinct decision-making scenarios in terms of dynamical system theory [27].

Results

A core model of the mammalian G1-phase regulatory network

The eukaryotic cell-cycle machinery. Eukaryotic cell cycle progression basically relies on a tight competition between two major players: cell-cycle activators and inhibitors. The model interaction graph shown in Figure 1B incorporates the main positive and negative regulators of G1 phase. Among cell-cycle activators are the cyclins D and E together with their Cdk4,6 and Cdk2 partners, respectively, and one subfamily of transcriptional factors termed activator E2Fs, which stimulate the transcription of genes involved in both cell division, notably cyclin E, and cell death [28]. The cell-cycle inhibitors included in our model are the members of the retinoblastoma (Rb) protein family that bind to and inhibit the activator E2Fs and the members of the Cip/Kip family of CKIs (p21Cip1, p27Kip1, p57Kip2).

Activatory and inhibitory G1-phase regulatory signals. Synthesis and accumulation of cell-cycle activators and inhibitors require the activation of two distinct types of pathways: (i) on the one hand, the continuous provisioning of growth factors (that is pooled into the control parameter \( I_{GF} \), where the GF index stands for growth factors) facilitates cyclin D synthesis and accumulation and the formation, activation and nuclear accumulation of cyclin D-Cdk4,6 complexes; (ii) on the other hand, genotoxic and cytotoxic stresses (e.g. DNA damage, depletion of nucleotide triphosphates, hypoxia, nutrient deprivation, cell-cell contact, oncogenic signals, cell deformation, …) as well as differentiation signals (that are pooled into the control parameter \( I_{SF} \), where the SF index stands for stress factors) facilitate the accumulation of CKIs. The present model does not take into account the influence of cell size and cell growth although cyclin-Cdks have been acknowledged both to regulate and be regulated by cell growth [29–31]. This is because we are interested here in understanding the behaviour of cells from multicelled species in which G1-phase progression is not limited by cell growth but rather by exogenous and endogenous stress signals [9].

Selective interactions between Rb proteins and G1-specific cyclin-Cdks complexes. Exit from G0 in mammalian cells is contingent upon growth factor-induced accumulation of cyclin D-Cdk4,6 whose first mission is to initiate Rb phosphorylation and, thereby, relieve the transcriptional repression of cyclin E genes by the Rb-E2F complexes [14]. Then, besides initiating the assembly and activation of replication complexes [32], the emerging cyclin E-Cdk2 complexes play a critical role, consisting in phosphorylating the Rb proteins whereby they free the activator E2Fs that activate a cohort of cell cycle-regulating genes and promote G1/S transit. Rb proteins, thus, can exist under three different phosphorylated forms, each of which exerts unique activities [15,33,34]: (1) unphosphorylated, they act as transcriptional repressors by inhibiting the activity of all three RNA polymerases [35], but also by selectively inhibiting the transcription of a number of genes, including cyclin E but not cyclin D, via the mobilization of chromatin-modifying factors [36]; (2) when partially (hypo)phosphorylated by cyclin D-Cdks, they lose their ability to directly repress transcription, including that of cyclin E; (3) when hyperphosphorylated by cyclin E-Cdk2, they dissociate from the
E2F factors, enabling them to stimulate the transcription of genes involved in both cell division and cell death, of which cyclin E.

Selective interactions between Cip/Kip proteins and G1-specific cyclin-Cdks. Cell-cycle arrest in G1 phase is mediated in great part by the p21/p27 members of the Cip/Kip family of CKIs, which bind to and inhibit the activity of all cyclin-Cdk1,2 complexes. The Cip/Kip proteins, in turn, are quickly downregulated upon phosphorylation by the cyclin-Cdk1,2 complexes, which indicates a strong mutually-antagonistic interaction between these two components. The interaction between Cip/Kip proteins and cyclin D-Cdk is more versatile and subject to controversy. On the one hand, Cip/Kip proteins bind to the cyclin D-Cdk complexes that they assemble and target to the nucleus without inhibiting their kinase activity [16,17]. On the other hand, it has been reported recently that context-dependent tyrosine-dephosphorylation of p27Kip1 can turn their activatory role into an inhibitory one [37,38]. In our standard model of G1-phase, Cip/Kip will be considered as an activator of cyclin D-Cdk although the alternative scenario will be also investigated upon modification of the model.

Cip/Kip-mediated inhibition of cyclin E-Cdk2 delays S-phase entry and induces G1 arrest

For the sake of simplification, it is convenient to consider that G1-phase progression relies on the contrasting activity of only two families of signals: (i) activatory signals, which promote cell division initially by facilitating the accumulation of cyclin D-Cdk4,6 and (ii) inhibitory signals, which oppose cell division by facilitating the accumulation of Cip/Kip proteins. In this case, indeed, the rate of G1-phase is expected to critically depend on the relative levels of the two competing signals. Figure 2 recapitulates how the combination of cell-cycle activatory and inhibitory signals may not only determine the outcome of G1-phase progression but also the timing of G1-phase events. We performed numerical calculations to simulate how G1-phase proceeds in response to a simultaneous step of growth factors and of stress factors applied at time $t_1$. S-phase entry is assumed to occur at time $t_s$ when the concentration of the activator E2Fs becomes larger than half its maximum value. Consistently with previous modeling studies and bifurcation analysis (Fig. S1A), G1/S transition is triggered via a bistable switching process. In this case, bistability is primarily generated by a positive feedback loop through which cyclin E-Cdk2 free the E2F factors from Rb proteins and, thereby, boost cyclin E synthesis and their own accumulation, though other Cdk2 free the E2F factors from Rb proteins and, thereby, boost S-phase entry and eventually induce a stable G1-arrest state when the ISF intensity reaches a critical value $IC_{C-}$. In order to assess whether this cell-cycle arrest is reversible, we performed numerical calculations to simulate how the G1-arrest state evolves when the ISF signal is gradually removed. We found that G1-phase progression is restored as soon as ISF falls below a critical value $IC_{C-}$ equal to $IC_{C+}$, hinting that the G1-arrest state is fully reversible (Fig. 3A).

It was reasonable to hypothesize that the reversible nature of mammalian G1 arrest takes root in the underlying mechanisms of G1-phase regulation, notably in the intricate relationship between the two G1-specific activatory modules and CKIs of the Cip/Kip family. Remind that G1-phase progression is governed by the sequential activation of cyclin D-Cdk4,6 and cyclin E-Cdk2 and that CKIs of the Cip/Kip family exert an opposite effect on cyclin D-Cdk4,6 and cyclin E-Cdk2. In order to test this hypothesis, we performed numerical calculations to simulate how G1-phase duration depends on ISF and evaluated $IC_{C-}$ and $IC_{C+}$ in two distinct hypothetical situations, in which: (1) Cip/Kip proteins inhibit the kinase activity of cyclin D-Cdk2 (Fig. 3B); (2) cyclin E transcription is not selectively repressed by unphosphorylated Rb (Fig. 3C). In the first situation, the plot depicting the rate of G1-phase progression ($1/t_{G1}$) as a function of ISF shows that $1/t_{G1}$ sharply decreases when ISF becomes close to $IC_{C+}$. Moreover, G1-phase progression is restored upon stress removal when ISF falls below a critical value $IC_{C-}$ equal to $IC_{C+}$, indicating that the G1-arrest state cannot be reversed for ISF values comprised between $IC_{C-}$ and $IC_{C+}$. In the second situation, $1/t_{G1}$ drops even faster when ISF gets close to $IC_{C+}$ and the ISF window in which irreversible G1 arrest occurs is still broader (Fig. 3C).

Besides the identification of strategic G1-phase regulatory features, the result of Fig. 3 underscores the existence of two poles apart decision-making scenarios according to whether $IC_{C-}$ is null (i.e., reversible case) or positive (i.e., irreversible case). To trace back the origin and the significance of these qualitative differences, we also perform bifurcation and sensitivity analysis for the standard and modified G1-phase models (see section A of Text S1). One the one hand, standard bifurcation
According to the terminology in Table 1, the concentrations shown are:

- IG
- G0-like state. Entry into S phase is assessed by the sharp rise of E2F at time $t_0$. G1-phase duration is defined as the time gap $t_{G1} = t - t_0$. Four combinations of signal intensities are considered: (a) $IG = 0.1, ISF = 0.1$; (b) $IG = 0.6, ISF = 0.1$; (c) $IG = 0.6, ISF = 0.2$; (d) $IG = 0.6, ISF = 0.5$. According to the terminology in Table 1, the concentrations shown are $[Rb] + [Rb\_E2F]$ (dashed line), $[Rb] + [Rb\_E2F]$ (dotted line), $[E1] + [D1]$ (dash-dotted line), $[E2F]$ (full line).

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There are two distinct bifurcation scenarios of limit cycles [27]: (i) a saddle-node bifurcation, which can be captured analytically when the parameter $IC$ of the decision fates and the standard deviations $\sigma_{fate}$ of the decision fates and the standard deviations $\sigma_{G1}$ of the decision times, which are defined as followed:

\[
\sigma_{fate} = \sqrt{\sum D_i^2 - \left( \sum D_i \right)^2}^{1/2}
\]

\[
\sigma_{G1} = \sqrt{\sum (\tau_{G1})^2 - \left( \sum (\tau_{G1}) \right)^2}^{1/2}
\]

where the $D$ value is equal to 1, if the final outcome is to enter S-phase, and 0, otherwise. For cells displaying the regulation scheme depicted in Figure 3A, all cells are likely to experience the same fate (except in a very small window), either S-phase entry or G1-phase arrest depending on the mean value of $IG$. Yet, when they progress towards S-phase entry, they do

Dynamical analysis of distinct mechanisms of G1-phase decision

The dynamical origin of the qualitative differences in G1 length tunability and G1-arrest reversibility unveiled in Figure 3 becomes apparent if one plots schematically the trajectory of G1-phase progression on an appropriate projection of the protein concentration space (Fig. 4). In normal proliferation conditions, the concentrations of the cell-cycle regulatory proteins evolve with time along a limit-cycle trajectory in the high-dimensional protein concentration space, more specifically on the G1-phase portion of the attractor landscape. This trajectory is slightly tunable and G1-arrest reversibility unveiled in Figure 3 becomes apparent if one plots schematically the trajectory of G1-phase progression in cells subjected to different ISF signals at time $t_0$. Figures 5A and B show how subtle changes in the mean value of ISF, at which the G1-phase trajectory arising from a mitotic or G0-arrest state converges to a G1-arrest state, may be equal to or larger than the critical value of $ISF$, at which the G1-arrest state is stabilized or destabilized. Extrapolating to the full cell cycle, these two examples of cell-cycle exit would correspond to two different bifurcation scenarios of limit cycles [27]: (i) a saddle-node bifurcation would occur on an invariant circle (called SNIC bifurcation) when $IC_{C} = IC_{C-}$; (ii) a saddle homoclinic bifurcation would occur at $IC_{C}$, when $IC_{C} > IC_{C-}$.

In these two distinct decision-making scenarios, the relationship between G1 length and $ISF$ can be captured analytically when the G1 length diverges for $ISF$ approaching $IC_{C}$ (see section B of Text S1):

\[
1/\tau_{G1} \propto \sqrt{IC_{C} - ISF}
\]

\[
1/\tau_{G1} \propto 1/\ln[IC_{C} - ISF]
\]

Noisy decision times versus noisy decision fates

Our study thus unveils how subtle differences in the organisation of the G1 regulatory network may nevertheless change drastically the property of G1-phase progression, especially whether G1-arrest state is reversible or irreversible like during senescent or terminally-differentiated state. We show in Figure 5 that cell populations subjected to noisy $IG$ signals statistically behave quite differently depending on the G1-regulatory scheme and G1-arrest strategy that prevail in individual cells. We simulated G1-phase progression in cells subjected to different temporal patterns of $ISF$ signal characterized nevertheless by the same mean and variance. We then measured the standard deviation $\sigma_{fate}$ of the decision fates and the standard deviations $\sigma_{G1}$ of the decision times, which are defined as followed:

\[
\sigma_{fate} = \sqrt{\sum D_i^2 - \left( \sum D_i \right)^2}^{1/2}
\]

\[
\sigma_{G1} = \sqrt{\sum (\tau_{G1})^2 - \left( \sum (\tau_{G1}) \right)^2}^{1/2}
\]

where the $D$ value is equal to 1, if the final outcome is to enter S-phase, and 0, otherwise. For cells displaying the regulation scheme depicted in Figure 3A, all cells are likely to experience the same fate (except in a very small window), either S-phase entry or G1-phase arrest depending on the mean value of $IG$. Yet, when they progress towards S-phase entry, they do
Table 1. Model equations and parameters.

Differential equations

| Differential equations                                                                 |   |
|----------------------------------------------------------------------------------------|---|
| \( \frac{d[GF]}{dt} = k_{GF} \frac{I_{GF}}{(k_{GF} + I_{GF})} - d_{GF}[GF] \)         |   |
| \( \frac{d[Rh]}{dt} = x_{Rh} - k_{Rh} + k_{E2F}[Rh] - d_{Rh}[Rh] \)                  |   |
| \( \frac{d[Rh, E2F]}{dt} = -k_{Rh} - k_{E2F} + (d_{E2F} + d_{Rh})[Rh, E2F] \)       |   |
| \( \frac{d[Rh, yp]}{dt} = -k_{Rh} + d_{Rh}[Rh, yp] \)                                |   |
| \( \frac{d[E2F]}{dt} = x_{E2F} + k_{E2F} + d_{E2F}[Rh, E2F] - d_{E2F}[E2F] \)       |   |
| \( \frac{d[D]}{dt} = x_{D}[D] + k_{D} - d_{D}[D] \)                                  |   |
| \( \frac{d[I]}{dt} = k_{I} - d_{I} \)                                                |   |

Dimerization/dissociation kinetic parameters

| Parameters                                                                 |   |
|---------------------------------------------------------------------------|---|
| \( v_{Rh} = 2 \text{mM}^{-1} \text{min}^{-1} \)                           |   |
| \( v_{2s} = 0.5 \text{mm}^{-1} \)                                         |   |
| \( v_{3s} = 0.5 \text{mm}^{-1} \)                                         |   |
| \( v_{Rh} = 4 \text{mM}^{-1} \text{mm}^{-1} \)                            |   |
| \( v_{D} = 0.4 \text{mM}^{-1} \)                                          |   |

Phosphorylation/dephosphorylation kinetic parameters

| Parameters                                                                 |   |
|---------------------------------------------------------------------------|---|
| \( k_{Rh} = 0.1 \text{mM} \)                                             |   |
| \( k_{Rh} = 0.4 \text{mM} \)                                             |   |
| \( k_{Rh} = 1.5 \text{mM} \text{mm}^{-1} \)                             |   |
| \( k_{Rh} = 1.5 \text{mM} \text{mm}^{-1} \)                             |   |
| \( k_{Rh} = 2 \text{mm}^{-1} \)                                          |   |
| \( k_{Rh} = 2 \text{mm}^{-1} \)                                          |   |
| \( k_{Rh} = 4 \text{mm}^{-1} \)                                          |   |
| \( k_{Rh} = 1 \text{mm}^{-1} \)                                          |   |

Synthesis/degradation kinetic parameters

| Parameters                                                                 |   |
|---------------------------------------------------------------------------|---|
| \( x_{GF} = 12 \text{mM h}^{-1} \)                                         |   |
| \( k_{GF} = 0.2 \text{mM} \)                                              |   |
| \( x_{GF} = 3 \text{mM h}^{-1} \)                                         |   |
| \( x_{E2F} = 3 \text{mM h}^{-1} \)                                         |   |
| \( k_{E2F} = 6 \text{h}^{-1} \)                                           |   |
| \( x_{E2F} = 12 \text{mM h}^{-1} \)                                        |   |
| \( k_{E2F} = 6 \text{h}^{-1} \)                                           |   |
| \( d_{E2F} = 0.05 \text{mM h}^{-1} \)                                    |   |
| \( d_{E2F} = 0.3 \text{h}^{-1} \)                                         |   |
| \( d_{E2F} = 27 \text{h}^{-1} \)                                          |   |
| \( d_{E2F} = 0.3 \text{h}^{-1} \)                                         |   |

Dynamic equations and parameters associated with the network shown in Figure 1B. There are 12 variables, 31 kinetic parameters and 2 input-dependent control parameters (k_{Rb} and k_{Ia}). J: Cip/Kip; D: cyclin D-Cdkis; E: cyclin E-Cdkis.
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so at a highly variable rate (left panels of Fig. 5B and C). Contrastingly, in the situation corresponding to the regulation scheme combining those depicted in Figure 3B and C, cells are prone to experience different fates for a broad range of (right panel of Fig. 5A) and those which progress towards S-phase entry tends to display a G1 phase of equal length as assessed by the low \( \sigma_{G1} \) value and the temporal profile of Cip/Kip proteins in various cells (right panels of Figs. 5B and C). It is worth to mention that similar results are obtained by considering intrinsic molecular noises instead of noises in input signals. Thus, fluctuations, extrinsic or intrinsic, can produce either noisy decision times or rather noisy decision fates depending on the particular G1-phase regulatory scheme. Our result suggests that the G1-phase organization of mammalian cells (left panels of Fig. 5) would favor fate reliability over fast decisions, which makes sense since cells in multicellular organisms are exempt from the imperative to divide rapidly and must avoid inappropriate decisions that may perturb the homeostasis of their host as in tumorigenesis.

Discussion

Design features of mammalian G1-phase flexibility

Whereas the core cell division process is strongly conserved amongst eukaryotes, entry in and progression through G1 phase follow a highly changeable course depending on cell type and environmental cues. In that phase, mammalian cells are submersed with an abundance of conflicting signals, competing with each other to encourage cell fates as irrecducible as cell division, differentiation, senescence and death [9,13]. In that phase also, like in G2, cells are required to repair DNA damages and replication errors committed in S phase. It is not astonishing therefore that mammalian cells have evolved an exceedingly complex web of molecular interactions to control in a contextual
It is reasonable to postulate that the acquired ability of mammalian cells to elaborate flexible G1 phases, especially during developmental processes, takes root in the architecturing of their G1 regulatory network. We therefore developed a dynamical modeling approach with the aim to check the role that could play on G1-phase control two especially striking G1 regulatory elements: (i) the selective transcriptional repression of cyclin E by unphosphorylated Rb proteins in very early G1 phase [14,15,36], which operates to delay the apparition of the cyclin E-Cdk2 complexes after growth-factor stimulation; (ii) the opposite effect on cyclin D-Cdk4,6 and cyclin E-Cdk2 of the Cip/Kip proteins, which, following their accumulation in response to stress signals and stockpiling of Cip/Kip proteins depends on the stress signals and stockpiling of Cip/Kip proteins.

Figure 3. Features of G1-phase regulation responsible for tunable G1 length and reversible G1 arrest. Three different situations have been analysed (Top panels): (A) the standard one corresponding to Figure 1 (see Table 1) and two hypothetical ones in which: (B) the Cip/Kip proteins inhibit the activity of cyclin D-Cdk4,6 \( (k_{d4,6} = 0 \text{mM}^{-1}, k_{d4,6} = 4 \text{mM}^{-1}) \) and (C) unphosphorylated Rb proteins does not repress cyclin E transcriptions \( s_{E,0} = 0 \mu M^{-1} \) that is compensated by reducing \( s_{E,0} \) and \( s_{E,0} \) by 70%. Bottom panels: plots depicting the changes in the rate of G1-phase progression (1/\( t_{G1} \)) as a function of \( I_{SF} \) starting from the G0 state \( (I_{SF} = I_{SF} = 0) \), when G0 exit is triggered by an \( I_{SF} \) step equal to one (like in Fig. 2). Grey filled and hatched regions define \( I_{SF} \) intensities for which the G1-arrest state is stable. Hatched regions bounded by \( I_{SF} \) and \( I_{SF} \) specify \( I_{SF} \) intensities for which G0-arrested cells are able to progress toward S-phase entry following growth factor stimulation but for which G1-arrested cells fail to return to the cell cycle following stress signal withdrawal.

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Flexible Control of Mammalian G1 Progression

Cip/Kip-mediated, exquisitely-sensitive control of G1-phase duration in mammalian cells

Our finding that a moderate increment in Cip/Kip proteins lengthens G1 phase is a priori not surprising and it has already been documented in several experimental studies [39,40]. Yet, it has not been realized before that the ability of mammalian cells to finely tune their G1 length in response to various constant levels of stress signals and stockpiling of Cip/Kip proteins depends on the contrasting way how distinct G1-specific cyclin-Cdks are regulated by the same entities (unphosphorylated Rb proteins and Cip/Kip proteins), which provides mammalian cells with an extremely powerful avenue to control their rate of G1-phase progression according to both the specificity of cell-cycle inhibitory stimuli and the relative strength of activatory and inhibitory cell-cycle regulatory signals. This result is not only supported by numerical experiments but also by dynamical system analysis that predicts an approximate square-root relationship between the rate of G1 progression and the strength of antimitogenic signals. Although no quantitative data are available to assess this prediction, this could nevertheless account for the huge G1-length variability observed in the course of development in multicellular organisms. In early embryos, cells can proceed through continuous S-M cycles in a mere half hour, paced by the oscillations in the activity of the universal mitosis-specific cyclin-Cdk1 module. As embryogenesis unfolds, however, a G1 delay is incorporated between M and S phases, giving time to cells to integrate a wealth of environmental signals whose distribution may be spatially organized and, accordingly, to commit to divide at appropriate times in coordination with their neighbours. As a matter of fact, it has been reported that, in embryonic neural and hematopoietic stem cells, the decision whether to differentiate or not, correlates with G1-phase duration [11,12]. Therefore, the ability of mammalian cells to elaborate exceedingly flexible G1 phases of great variability in length is crucial to generate tissue diversity and ensure coordinated tissue development during embryogenesis [11,41]. Our study further suggests that this evolutionary capacity may originally stem from the emergence, upon the pressure of environmental constraints, of an early G1-specific cell-cycle activatory module, namely the cyclin D-Cdk module, distinct from the universal mitosis-specific cyclin-Cdk module inherited from unicelled organisms and differently regulated by CKIs.
Cip/Kip-dependent reversible versus irreversible G1 arrest

It has long been recognized that accumulation of the Cip/Kip proteins in response to genotoxic and cytotoxic stress signals eventually leads to G1 arrest by inhibition of the cyclin E-Cdk2 complexes [42]. Actually, many Cip/Kip-inducing signals have been reported to give rise to reversible G1 arrest, on account of the fact that, upon stress removal, cell cycle progression could be restored [43–49]. The rigorous demonstration, however, that such stimuli are truly able to induce fully reversible G1 arrests would require to check whether indeed hysteresis does not occur in experiments in which the stress signal level would gradually be reduced, which is difficult to achieve in practice. Cip/Kip proteins have been acknowledged also to contribute to the establishment of irreversible cell-cycle arrests, for instance in response to differentiation signals or in senescent cells [50]. Our study predicts that, converting Cip/Kip-mediated G1 arrest from reversible to irreversible requires additional modules, besides those included in Figure 1B, to participate in G1-phase regulation. It is noteworthy that human fibroblasts undergoing replicative senescence in culture typically accumulate a number of markers which appear to be causally involved in the onset of senescence, including the p53 tumor suppressor protein and one of its main downstream effectors, p21Cip1, but also p16Ink4a [51,52]. The Ink4a proteins selectively bind Cdk4,6, blocking the assembly of cyclin D-Cdks.

Figure 4. Dynamical mechanisms underlying distinct G1-phase decisions. (A) Schematic representation of how the ISF signal modifies the trajectories of G1-phase progression in the state space in the case of reversible (left panels) and irreversible (right panels) G1-arrest states. Black circles and white circles indicate a stable equilibrium linked to a G1-arrest state and an unstable equilibrium, respectively. Half black and half white circle indicates a saddle-node equilibrium. Left and right panels correspond to two qualitatively distinct scenarios. In case of limit cycle trajectories (connecting S to M), panels (a) and (b) would correspond to a saddle-node bifurcation on invariant cycle and a saddle homoclinic bifurcation, respectively. (B) Typical asymptotic relationship between the rate of G1-phase progression ($1/\tau_{G1}$) and ISF strength associated with reversible and irreversible G1-arrest scenarios (see supporting material). doi:10.1371/journal.pone.0035291.g004

Figure 5. G1-phase decision variability in presence of fluctuating stress signals. (left panels): standard scenario that gives rise to a reversible G1-arrest state and corresponding to the scheme depicted in Figures 1 and 3A. (right panels): scenarios giving rise to irreversible G1 arrest, combining the schemes depicted in Figures 3B and 3C. Numerical simulations were performed on several hundreds of cells subjected to different $I_{SF}(t)$ signals with the same mean $<I_{SF}>$ and the same coefficient of variation of 29%. In fact, $I_{SF}$ switches every 5 min between uniformly distributed random values. (A,B) Plots of $\sigma_{\text{late}}$ and $\sigma_{\text{G1}}$, respectively, as a function of $<I_{SF}>$. (C) Time course of $[\text{Cip/Kip}]$ in 10 cells subjected to an average stress input $<I_{SF}>$ indicated by the dashed line in panels A and B. Asterisks indicate the S-phase entry event (G1/S transition). doi:10.1371/journal.pone.0035291.g005

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and, thus, preventing accumulation of cyclin D-Cdk4 and sequestration of the Cip/Kip proteins in the early stages of G1 phase. According to our study, stress signals favoring the synthesis and accumulation of p16Ink4a, and p21Cip1-inducing stress signals could therefore cooperate to induce irreversible G1 arrests. Interestingly too, it has been reported recently that p27Kip1 fails to inhibit cyclin D-Cdk4,6 only following tyrosine-phosphorylation in its N terminal domain [37,38]. Thus, context-dependent tyrosine-dephosphorylation of p27Kip1 could offer to mammalian cells a means to shift from a reversible to an irreversible G1-arrest state.

From cell-cycle models to decision-making theory

A major challenge for science in the twenty-first century is to develop an integrated understanding of how cells and organisms survive and reproduce [53]. In this huge task, modeling approaches that attempt to extract biological design and dynamic principles will certainly prove of great help. Modeling G1-phase regulation is especially appealing for theoreticians because G1 phase is a critical period of the cell cycle during which individual cells make crucial decisions concerning the organism as a whole. In the search for design principles of G1-phase regulation, the present modeling study identifies a subset of singularities that appear to play a paramount role in the temporal control of G1-phase progression but that were dismissed in previous models. It should be kept in mind, however, that the core set of regulations included in our model is embedded within an exceedingly complex web of signalling and regulatory pathways, which work in concert to coordinate cell growth, cell division, cell differentiation, stress management and survival [9]. An important step forward would be to integrate and reconcile together the multitudinous theoretical works that have already analysed in detail one or another aspect of mammalian G1-phase regulation, e.g. the restriction point [20,22,25,26] or the crosstalk between pathways controlling various cell fates [24,54,55]. Models of G1-phase regulation are thus an inexhaustible playground to investigate decision-making properties in terms of reversibility, timing or stochastic, which could be extrapolated to other decision-making systems. In particular, the selection between alternative decision strategies - reversible, irreversible or hybrid - may be relevant not only for other cell-cycle arrest decisions [55,56], but more generally for any biological processes involving sequential choices, such as during cellular differentiation [57,58], neuronal spiking [59] or brain cognition [60,61], thereby manifesting universal principles of biological decision making.

Methods

Mathematical model equations

The molecular processes subsumed under the G1 regulatory network defined in the first section of the result section and illustrated in Figure 1B are described by a set of differential equations according to the standard principles of biochemical kinetics (Table 1). Thus, the dynamical properties of the mathematical model are are represented by 12 differential equations describing the time-dependent changes in concentrations of individual components of the network occurring following their modification via a variety of biochemical processes including transcriptional activation/repression, translation, degradation, phosphorylation, dephosphorylation, association, dissociation. The phosphorylation/dephosphorylation reactions are supposed to follow the Michaelis-Menten kinetics [21]. A number of assumptions have been made to restrict the quantity of variables: (i) several proteins (e.g, Cdc25, Myc, p33, Ink4) that are sometimes included in other G1-phase models [21,25,26,55], are omitted in our own model because our interest was more specifically focusing on the interplay between, on the one hand, the cyclin D,E-Cdk activatory modules and, on the other hand, the Rb/E2F and Cip/Kip regulatory modules ; (ii) we did not discriminate between the different members of the Cip/Kip, Rb or E2F protein family, which are generally supposed to play similar, redundant roles though in different contexts; (iii) mRNA-regulatory or translocation processes are also disregarded in our model; (iv) the effect of cell growth is neglected as well because cell growth is presumed to have a limited impact on G1-phase progression in somatic cells from multicelled species. The differential equations used to simulate the G1 regulatory network model were integrated using the second-order Runge-Kutta scheme with fixed-time step \( dt = 0.005 \).

Choice of kinetic parameters

Like in most previous models of the cell cycle, the choice of parameters is mostly arbitrary because of the lack of data regarding the rate constants of the physiological reactions that participate in the G1 regulatory network and, also, because we were interested before all on the phenomenological features of the network dynamics. Consistently with the literature, the cyclin half-life is assumed to be shorter than those of the Cip/Kip and E2F proteins that themselves are assumed to be shorter than the halftime of Rb proteins. All parameter values are indicated in Table 1 and their possible changes in the course of the study are specified in the captions. Parameter sensitivity analysis shown in Figure S2 and described in supporting material confirms that the precise choice of kinetic parameters is not critical for the validity and the significance of our results as the qualitative properties of the model are robust to reasonable changes of model parameters.

Supporting Information

Text S1  Dynamic analysis of G1-phase models and G1-length tunability.

(PDF)

Figure S1  Bifurcation analysis. Bifurcation diagram showing normalized steady state E2F activity as a function of IC for IC = 0 (A and C) and as a function of IC for IC = 0.6 (B and D). Three G1-phase models depicted in supporting material or in Figure 3 are shown: the model A (A and B) and the models B and C (respectively blue and red of C and D). Solid and dashed lines are associated with stable equilibria and saddle equilibria, respectively. White circles highlight saddle-node bifurcation points for which IC = \( \theta_{IC} \) (destabilization of the G0 state) and IC = IC (stabilization of the G1-arrest state).

(EPS)

Figure S2  Parameter sensitivity analysis. Plot of \( \theta_{IC} \), IC, and IC as a function of the normalized hysteresis size (IC - IC)/IC for model A (black crosses), B (red circles) and C (blue squares) in which all model parameters are multiplied with a factor of 1.3 and 0.7.

(EPS)

Figure S3  Asymptotic laws for G1-length tunability. Plot of \( 1/t_{G1} \) as a function of IC - IC represented in log-log scale for the three G1-phase models: (A) For the model A, the relationship between \( 1/t_{G1} \) and IC = IC - IC can be fitted with a square root function \( (a=0.7) \) for enough small values of IC. (B) For models B and C, the relationship between \( 1/t_{G1} \) and IC = IC - IC can be fitted with the inverse of a logarithm function \( (Model \ B: a=4.2 \ and \ b=2.3; \ Model \ C: a=9.5 \ and \ b=0.5) \).

(EPS)
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