IceCube Events from Heavy DM decays through the Right-handed Neutrino Portal

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Abstract

The recently observed IceCube PeV events could be due to heavy dark matter (DM) decay. In this paper, we propose a simple DM model with extra $U(1)_X$ gauge symmetry and bridge it with standard model particles through heavy right-handed neutrino. The Dirac fermion DM $\chi$ with mass $\sim 5\text{ PeV}$ can dominantly decay into a dark Higgs ($\phi$), the SM Higgs ($h$) and a neutrino ($\nu$). If the lifetime of $\chi$ is $\sim O(10^{28})$ sec, the resulting neutrino flux can fit data consistently. The neutrino flux from $\chi \rightarrow \phi h \nu$ in our model is softer than the one predicted from $\chi \rightarrow \nu h$, for example. We also discuss a possible mechanism to produce DM with the right relic abundance.
I. INTRODUCTION

Recently, the IceCube Collaboration has reported the detection of 37 neutrino events with energy between 30 TeV − 2 PeV, of which three have energy above 1 PeV [1–3]. According to the recent analyses [4–7], the three-year data are consistent with equal fluxes of all three neutrino flavors and with isotropic arrival directions. However, the neutrino flux required to fit the data in 100 TeV − PeV range is around $10^{-8}$ GeV cm$^{-2}$s$^{-1}$sr$^{-1}$ per flavor, and rejects a purely atmospheric explanation at 5.7$\sigma$. Therefore astrophysical and/or new physics explanations have been pursued for the origin of these high energy neutrinos.

Possible astrophysical sources are involved with supernova remnants (SNR) [8–12], active galactic nuclei (AGN) [13–16], and gamma-ray bursts (GRB) [17, 18], all of which assume some specific emission spectra due to different production environments. In a model independent analysis, the best-fit power law spectrum from the IceCube analysis [1] is $E_\nu^2d\Phi_\nu/dE_\nu \simeq 1.5 \times 10^{-8}(E_\nu/100 \text{ TeV})^{-0.3}$ cm$^{-2}$ s$^{-1}$sr$^{-1}$. It is not very straightforward to fit such a spectrum by astrophysical sources. In all cases, extragalactic sources are needed due to the isotropic feature and galactic constraints [19–22]. Then identifying such astrophysical sources will be crucial for further understanding of IceCube events.

Dark matter (DM) and other new physics interpretations have been also investigated in various ways or models. Heavy DM might decay into SM particles that give energetic PeV neutrinos [23–37] 1, or it could decay into some light DM particles which interact with nucleons and mimic neutrino events [39, 40]. The resulting neutrino flux would still be consistent with isotropy so far, since galactic and extragalactic DM contribute at the similar order. One unique feature of DM explanation is that there should be sharp energy cut-off in the neutrino spectrum, which could be tested by future data. Also, a possible gap around 400 TeV $\sim$ 1 PeV, although not statistically significant yet, motivated considerations of new interactions, two-component flux and leptophilic DM decay [32, 41–47].

In this paper, we propose a simple DM model to explain the IceCube PeV events. A dark sector with new $U(1)_X$ gauge symmetry is introduced and can have connection with the standard model (SM) sector through neutrino-portal interactions as well as the Higgs portal interaction. Fermionic DM (\(\chi\)) has $\sim$ PeV mass and mostly decays into three-body final state with dark Higgs (\(\phi\)), SM Higgs (\(h\)) and active neutrino. The produced neutrinos from primary \(\chi\) decay and the secondary \(h\) and \(\phi\) decays can explain the observed PeV event spectra, while the atmospheric and astrophysical neutrinos are included for the low-energy part.

This paper is organized as follows. In Section. II we introduce our DM model with dark $U(1)_X$ gauge symmetry, heavy right-handed neutrino portal and Higgs portal interactions. In Section. III we outline the general formalism for calculating neutrino flux from galactic and extragalactic DM decay. In Section. IV we present both total and differential decay width for the relevant three-body decay in our model and compare the numerical results with IceCube data. In Section. V we discuss a possible mechanism to generate the correct relic density for DM and direct/indirect detection constraints. Finally, we give our conclusions.

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1 If involving of dark halo substructure, Ref. [38] showed annihilating DM scenario may also be possible.
II. MODEL

We consider a dark sector with a dark Higgs field $\Phi$ and a Dirac fermion DM $\chi$ associated $U(1)_X$ gauge symmetry. Their $U(1)_X$ charges are assigned as follows:\(^2\)
\[(Q_\Phi, Q_\chi) = (1, 1).\]

We begin with the following renormalizable and gauge invariant Lagrangian including just one singlet right-handed (RH) neutrino $N$ and one lepton flavor (more $Ns$ and/or flavors can be easily generalized):
\[
\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \bar{N}i\hat{D}N - \left(\frac{1}{2}m_N N^c N + y\bar{L}HN + \text{h.c.}\right) - \frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{1}{\sqrt{2}}\sin \epsilon X_{\mu\nu}F_{Y}^{\mu\nu} + D_\mu \Phi^\dagger D^\mu \Phi - V(\Phi,H) + \bar{\chi} (i\hat{D} - m_\chi) \chi - (f\bar{\chi}\Phi N + \text{h.c.}),
\]
(2.1)

where $L = (\nu l)^T$ is a left-handed (LH) SM $SU(2)$ lepton doublet, $H$ is the SM Higgs doublet, $X_{\mu\nu} = \partial_\mu X_\nu - \partial_\nu X_\mu$ is the field strength for $U(1)_X$ gauge field $X_\mu$, $F_{Y}^{\mu\nu}$ is for SM hypercharge $U(1)_Y$, and $\epsilon$ is the kinetic mixing parameter. Two types of Yukawa couplings, $y$ and $f$, can be taken as real parameters, ignoring CP violation for simplicity. We define covariant derivative as $D_\mu = \partial_\mu - igX_\mu$. Since we are interested in explaining the IceCube PeV events in terms of DM $\chi$ decay, we shall take $m_\chi \sim \text{PeV}$. Other parameters in our model are free variables.

The scalar potential $V$ of this model is given by
\[
V = \lambda_H \left(H^\dagger H - \frac{v_H^2}{2}\right)^2 + \lambda_\phi H \left(H^\dagger H - \frac{v_H^2}{2}\right) \left(\Phi^\dagger \Phi - \frac{v_\phi^2}{2}\right) + \lambda_\phi \left(\Phi^\dagger \Phi - \frac{v_\phi^2}{2}\right)^2,
\]
(2.2)

Both electroweak and dark gauge symmetries are spontaneously broken by the nonzero vacuum expectations values of $H$ and $\Phi$: $\langle H \rangle = (0, \frac{v_H}{\sqrt{2}})^T$, $\langle \Phi \rangle = \frac{v_\phi}{\sqrt{2}}$. Here $v_H \approx 246\text{GeV}$ is the same as SM value but $v_\phi$ might be taken as a free parameter. In the unitarity gauge, we can replace the scalar fields with
\[
H \rightarrow \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_H + h(x) \end{pmatrix} \quad \text{and} \quad \Phi \rightarrow \frac{v_\phi + \phi(x)}{\sqrt{2}}.
\]
(2.3)

Note that $h$ and $\phi$ shall mix with each other thanks to the Higgs-portal operator, (the $\lambda_{\phi H}$ term)\(^3\). Through this mixing, $\phi$ can decay into SM particles. Another important mixing happens among three neutral gauge bosons, photon $A_\mu$, $Z_\mu$ and $X_\mu$. Such a mixture would enable an extra mass eigenstate $Z'_\mu$ (mostly $X_\mu$) to decay SM fermion pairs. Then DM $\chi$ scattering off nucleus is possible by the $Z'$ exchange, and the cross section essentially depends on $\epsilon, v_\phi, m_{Z'}$. It is easy to choose small $\epsilon$, or heavy masses to evade the constraints from DM direct detection [54].

When the right-handed neutrino $N$ is much heavier than $\chi$, we can integrate it out and obtain an effective operator,
\[
\frac{yf}{m_N} \bar{\chi} \Phi H^\dagger L + \text{h.c.},
\]
(2.4)

\(^2\)A similar setup with different dark charge assignments has been considered for the AMS02 positron excess [48]. One may also use discrete symmetries, see Ref. [49] for example.

\(^3\)The $\lambda_{h\phi}$ term can also help to stabilize the electroweak vacuum [50–53].
which would make $\chi$ decay possible but long lived. After spontaneous gauge symmetry breaking, we have several higher dimensional effective operators from the aforementioned operator Eq. (2.4) as follows:

\[ \frac{v_\phi v_H}{m_N} \bar{\chi} \nu, \quad \frac{v_\phi}{m_N} \bar{\chi} h \nu, \quad \frac{v_H}{m_N} \bar{\chi} \phi \nu, \quad \frac{1}{m_N} \bar{\chi} \phi h \nu, \]

(2.5)

with the common factor $\frac{y_f}{2}$ for all these operators. If kinematically allowed, all the above operators induce $\chi$ decays into different channels with fixed relative branching ratios. Within the heavy $\chi$ limit, $m_\chi \gg m_\phi, m_{Z'}, m_h, m_Z, m_W$, the mass operator $\bar{\chi} \nu$ in Eq. (2.5) would induce a tiny mixing between $\chi$ and $\nu$ with the mixing angle $\beta$ approximately given by

\[ \beta \simeq \frac{y_f}{2} \frac{v_\phi v_H}{m_N m_\chi}. \]

(2.6)

Then the gauge interactions for $\chi$ and $\nu$ will generate the decay channels,

\[ \chi \rightarrow Z' \nu, Z \nu, W^\pm l^\pm, \]

(2.7)

with their branching ratios being proportional to $\sim v_H^2 : v_\phi^2 : 2 v_\phi^2$. Two dim-4 operators, $\bar{\chi} h \nu$ and $\bar{\chi} \phi \nu$, would lead $\chi$ to the following decays,

\[ \chi \rightarrow h \nu, \phi \nu, \]

(2.8)

with their branching ratios being proportional to $\sim v_\phi^2 : v_H^2$. It is also straightforward to get the following relation for the branching ratios,

\[ Br(\chi \rightarrow \phi \nu) : Br(\chi \rightarrow Z' \nu) \simeq 1 : 1. \]

(2.9)

Therefore, all the decay branching ratios are basically calculable and completely fixed in this model. Note that the decay modes with $Z'$ or $\phi$ are unique features of DM models with dark gauge symmetries.

Another interesting phenomenon in this model is that three body decay channel $\chi \rightarrow \phi h \nu$ is dominant over all other channels when $m_\chi \gg v_\phi$:

\[ \frac{\Gamma_3 (\chi \rightarrow \phi h \nu)}{\Gamma_2 (\chi \rightarrow h \nu, \phi \nu)} \simeq \frac{1}{16 \pi^2} \frac{m_\phi^2}{v_\phi^2 + v_H^2} \gg 1, \]

(2.10)

since we actually have an enhancement from heavy $m_\chi$ even though there is a phase space suppression from three-body final states. There are another three-body decay channels that are equally important:

\[ \chi \rightarrow \phi/Z' + h + \nu, \phi/Z' + Z + \nu, \phi/Z' + W^\pm + l^\mp, \]

with branching ratios $1 : 1 : 2$ due to the Goldstone boson equivalence theorem. In the following, if not otherwise stated explicitly, we use $\chi \rightarrow \phi h \nu$ to represent all these channels and in numerical calculations we take all of them into account.

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4 This is also true in the model for the AMS02 positron excess [48].

5 This is also true of three-body decays of DM discussed in the following paragraph.
To give a rough impression for the relevant parameter ranges, we can perform an order-of-magnitude estimation (complete formulas and details of calculation are given in the Appendix):

$$
\Gamma_3 (\chi \rightarrow \phi h \nu) \sim \frac{m_3^3}{96\pi^3} \left( \frac{y f}{m_N} \right)^2 \sim \frac{1}{10^{28} \text{sec}}
$$

$$
\Rightarrow \frac{y f}{m_N} \sim 10^{-36} \text{GeV}^{-1},
$$

which shows the required value for the combination $y f / m_N$. If one additionally assumes that $N$ should be responsible for neutrino mass through the usual Type-I see-saw mechanism, then we have $y \sim 10^{-5}$ and $f \sim 10^{-22}$ for $m_N \sim 10^{14} \text{GeV}$ and, $y \sim 10^{-5}$ and $f \sim 10^{-25}$ for $m_N \sim \text{PeV}$. In any case, $f$ is very tiny and seems unnaturally small. However, it is still natural a la ’t Hooft [55] since taking $f = 0$ enhances symmetries of the theory, namely DM number conservation 6. In later discussion, we shall take $y, f, m_N$ as free parameters, unless specified.

III. NEUTRINO FLUX FROM DM DECAY

The neutrino flux from dark matter decay is composed of galactic and extragalactic contributions which are equally important as we shall see below. Galactic neutrino flux at kinetic energy $E$ from DM decay in our Milky Way dark halo is given by

$$
\frac{d\Phi^G_\nu}{dE_\nu} \bigg|_{E_\nu = E} = \frac{1}{4\pi} \sum_i \Gamma_i \int_0^\infty dr \frac{\rho^G_\chi (r')}{m_\chi} \frac{dN^i_\nu}{dE_\nu} \bigg|_{E_\nu = E},
$$

where $\Gamma_i$ is partial width for decay channel $i$, $dN^i_\nu/dE_\nu$ is the neutrino spectrum at production, $r' = \sqrt{r_\odot^2 + r^2 - 2r_\odot r \cos \theta}$, $r$ is the distance to earth from the DM decay point, $r_\odot \approx 8.5 \text{kpc}$ for the solar system and $\theta$ is the observation angle between the line-of-sight and the center of the Milky Way. For the galactic DM density distribution, we use the following standard NFW profile [56],

$$
\rho^G_\chi (r') = \rho_\odot \frac{[r_\odot/r']}{[1 + r_\odot/r_c]} \left[ \frac{1 + r_\odot/r_c}{1 + r'/r_c} \right]^2,
$$

with parameters $r_c \approx 20 \text{kpc}$ and $\rho_\odot \approx 0.4 \text{GeV/cm}^3$. For decaying dark matter the flux is not very sensitive to DM density profile, so our discussions and results will still apply if another different profile is used.

We can also get the extragalactic or cosmic contribution from a formula similar to the above one, by taking cosmic expansion into account, namely the red-shift effect [24]:

$$
\frac{d\Phi^EG_\nu}{dE_\nu} \bigg|_{E_\nu = E} = \frac{\rho_c \Omega_\chi}{4\pi m_\chi} \sum_i \Gamma_i \int_0^\infty dz \frac{dN^i_\nu}{dE_\nu} \bigg|_{E_\nu = (1+z)E},
$$

where $E'$ is red-shifted to $E$ as $E' = (1+z)E$, the red-shift $z$ is defined as $1 + z = a_0/a$ with present scale factor $a_0$ being normalized to 1, the critical energy density $\rho_c = 5.5 \times$

6 The DM current $j^\mu_\chi = \bar{\chi} \gamma^\mu \chi$ is conserved in the limit $f \to 0$. 
FIG. 1. Neutrino spectra from DM $\chi$ decay with $m_\chi \sim 5$ PeV and lifetime $\tau_\chi = 1/\Gamma \sim 2 \times 10^{28}$ s. The left panel shows individual contribution of different final states from $\chi$’s decay, $\nu$ (blue dot-dashed curve) and $h/\phi$ (red dashed curve), respectively. The right panel presents the galactic (blue dashed curve) and extragalactic (red dot-dashed curve) neutrino flux.

$10^{-6}$GeV/cm$^2$ and $\Omega_\chi \simeq 0.27$ is DM $\chi$’s fraction. The Hubble parameter $H$ is related to its present value through

$$H = H_0 \sqrt{\Omega_\Lambda + \Omega_m (1+z)^3 + \Omega_r (1+z)^4},$$

$\Omega_\Lambda$, $\Omega_m$ and $\Omega_r$ are energy fractions of dark energy, all matter, and radiations, respectively. We shall use the latest results from Planck [57] for numerical evaluation.

IV. NUMERICAL RESULTS

To compute the neutrino flux from DM decay, we first need to calculate the total and differential three-body decay width for $\chi \to \phi + h + \nu$. In the heavy $\chi$ limit, we have obtained the total width

$$\Gamma \simeq \frac{m_\chi^3}{768\pi^3} \left( \frac{yf}{m_N} \right)^2,$$

and normalized differential decay widths

$$\frac{1}{\Gamma} \frac{d\Gamma}{dE_\nu} \simeq 24E_\nu^2/m_\chi^3, \quad 0 < E_\nu < m_\chi/2,$$

$$\frac{1}{\Gamma} \frac{d\Gamma}{dE_h} \simeq 12E_h (m_\chi - E_h)/m_\chi^3, \quad 0 < E_h < m_\chi/2,$$

$$\frac{1}{\Gamma} \frac{d\Gamma}{dE_\phi} \simeq 12E_\phi (m_\chi - E_\phi)/m_\chi^3, \quad 0 < E_\phi < m_\chi/2.$$

The details of the calculation are given in the Appendix where complete formulas with nonzero mass parameters are also presented. The above differential widths are essential
ingredients to get the final neutrino flux. For example, \( \nu \) from different decay final states are given by

\[
\frac{dN}{dE} (x \to \nu) = \int \frac{1}{\Gamma} \frac{dN_{\nu}(E_x)}{dE} dE_x,
\]

where \( x = \nu, h, W, Z, Z', \phi \). Note that \( dN_{\nu}(E_x)/dE \) in the integrand can be calculated with \texttt{Pythia} \[58\] or \texttt{PPPC4DMID} \[59\].

In Fig. 1 we show the neutrino spectra. Just for illustration, we choose the mass of DM \( \chi \) around 5 PeV and its lifetime \( 2 \times 10^{28} \) s. The neutrino spectra are multiplied by \( E_\nu^2 \) in order to account for the energy dependence of the neutrino-nucleus cross section so that it might be compared with IceCube data more easily. The blue dot-dashed curve indicates the spectrum from final \( \nu \) in \( \chi \)'s decay and red dashed one marks \( h/\phi \)'s contribution. For simplicity, the mass of \( \phi \) has been chosen to be just as the SM Higgs mass. However, other choice does not affect our result much, since in the left panel of Fig. 1 we see that in the high energy part \( h/\phi \)'s contributions are basically negligible and it is the high energy part that explains the IceCube PeV events. In the right panel, we include the red-shifted effects and show both galactic (blue dashed) and extragalactic (red dot-dashed) contributions.

Next, we compare our model predictions with IceCube three-year data \[1\]. To parameterize the possible astrophysical neutrino fluxes at low energy, we consider either a broken power law (BPL) or unbroken power law (UPL) \[32\],

\[
J_0^{\text{BPL}}\frac{d\Phi_{\text{bkg}}}{dE_\nu} = E_\nu^2 \left(\frac{E_\nu}{100\text{TeV}}\right)^{-\gamma_1} \exp\left(-\frac{E_\nu}{E_0}\right),
\]

\[
J_0^{\text{UPL}}\frac{d\Phi_{\text{bkg}}}{dE_\nu} = E_\nu^2 \left(\frac{E_\nu}{100\text{TeV}}\right)^{-\gamma_2},
\]

where the first one has an exponential cut-off at energy scale \( E_0 \) which is chosen to be 125 TeV in agreement with the SNR results \[8\].

We illustrate in Fig. 2 with two different astrophysical flux choices. The low energy data are best fitted by varying \( J_0 \) and the spectral index \( \gamma \), but the high energy PeV data points are fit by DM decay. In the left panel, we have used \( J_0^{\text{BPL}} = 4.1 \times 10^{-8} \) GeV/cm\(^2\)/s/sr and \( \gamma_1 = 0 \) (red dot-dashed curve). In the right panel, we have used \( J_0^{\text{UPL}} = 1.3 \times 10^{-8} \) GeV/cm\(^2\)/s/sr and \( \gamma_2 = 0.7 \) (red dot-dashed curve). DM’s contributions and total flux are labeled with purple dashed and blue solid curves, respectively. As we can see in the figure, our model can agree with the PeV data. Also a gap could appear around 400 TeV although the current data can not tell existence of the gap is statistically significant. The feature for the DM decay spectrum is that there would be a sudden drop around \( E_\nu \approx m_\chi/2 \). As more data are accumulated, it should be possible to test our model in the future.

We should note that in our discussion \( J_0 \) and \( \gamma \) are just adjusted visually to be consistent with the low-energy data points. Dedicated investigation would require global fitting, which is beyond our scope here. Just for comparison, IceCube \[60\] gives the best-fit parameters of a single unbroken power law for neutrinos energies between 25 TeV and 2.8 PeV without DM contribution, \( J_0 = 6.7^{+1.1}_{-1.2} \times 10^{-8} \) GeV/cm\(^2\)/s/sr and \( \gamma = 0.5 \pm 0.09 \).

In Fig. 3, we also compare our model with the preliminary updated results \[61\] based on IceCube 4-year data which has already filled the gap a bit. Here we have only shifted to \( J_0^{\text{BPL}} = 5.6 \times 10^{-8} \) GeV/cm\(^2\)/s/sr and \( \tau_\chi \sim 1.5 \times 10^{28} \) s (left panel), and \( J_0^{\text{UPL}} = 2.1 \times 10^{-8} \) GeV/cm\(^2\)/s/sr and \( \tau_\chi \sim 2 \times 10^{28} \) s (right panel). In Fig. 4, we illustrate two cases, one with \( m_\chi = 8 \) PeV, \( \tau_\chi \sim 1.7 \times 10^{28} \) s, and the other \( m_\chi = 10 \) PeV, \( \tau_\chi \sim 1.5 \times 10^{28} \) s.
FIG. 2. Neutrino flux from DM $\chi$’s decay with $m_\chi \sim 5$PeV and lifetime $\tau_\chi = 1/\Gamma \sim 2 \times 10^{28}$ s and IceCube Data [1]. The left (right) panel used a broken (unbroken) power law (BPL) for astrophysical neutrino flux with a red dot-dashed curve. DM’s contributions and total flux are labeled with purple dashed and blue solid curves, respectively. See details in the text.

FIG. 3. Same as Fig. 2 but with preliminary updated results based on 4-year data [61], with $J_0^{BPL} = 5.6 \times 10^{-8}$GeV/cm$^2$/s/sr and $\tau_\chi \sim 1.5 \times 10^{28}$ s (left), and $J_0^{UPL} = 2.1 \times 10^{-8}$GeV/cm$^2$/s/sr and $\tau_\chi \sim 2 \times 10^{28}$ s (right).

There are some crucial differences between our model and some others in the literature. For example, the authors in Ref. [23, 29] considered the effective operator, $y \bar{\nu} L \tilde{H} \chi$ with $y \sim 10^{-30}$, which induces mainly two-body decay of DM $\chi$,

$$\chi \rightarrow \nu h, \nu Z, l^\pm W^\mu.$$ 

In this scenario, the neutrino spectrum shows that there should be no gap between 400 TeV $\sim$ 1 PeV [26]. Our model predicts that the dominant decay mode are

$$\chi \rightarrow \phi/Z' + h + \nu, \phi/Z' + Z + \nu, \phi/Z' + W^\pm + l^\mp,$$
which is a consequence of $U(1)_X$ dark gauge symmetry and the dark charge assignments of the dark Higgs and dark matter fermion $\chi$. The neutrino spectra from primary $\chi$ decay and the secondary decays of $h$ and $\phi$ have different shapes and could account for the possible gap. However, we should note that the current data can not favor one over another yet due to its low statistics. Also the neutrino flux in our model is softer than the one predicted in Ref. [23, 29], for example.

In Ref. [32], leptophilic three-body decay induced by dimension-six $\bar{L}_\alpha l_\beta \bar{L}_\gamma \chi$ was considered with global $U(1)$ or $A_4$ flavor symmetries. Besides the neutrino spectrum difference, our model involves an additional gauge boson which mediates the DM-nucleon scattering, and could be tested by DM direct searches.

Our scenario is also different from those in which DM decay is also responsible for the low-energy flux [24]. The DM lifetime in Ref. [24] should be around $2 \times 10^{27}s$, as mainly determined by the low energy part of events. This is partly due to the reason that the branching ratio into neutrinos and $b\bar{b}$ there should be about 10% and 90%, respectively, to account for the possible gap. On the other hand, in our scenario 1/2 of the decay channels have prompt neutrinos. Another main difference is that three-body-decay usually gives broader spectra at PeV range than two-body-decay considered in Ref. [24], but more data is required in order to discriminate this difference.

Assuming the dark photon $X_\mu$ is much heavier than $Z$, the DM-nucleon scattering cross section can be roughly estimated as

$$\sigma_{\chi N} \sim \left(\frac{m_Z^2}{m_X^2}\right)^2 \sin^2 \epsilon \times 10^{-39}\text{cm}^2.$$  

$10^{-39}\text{cm}^2$ is the typical cross section value for SM $Z$-mediating DM-nucleon process. Comparing it with the direct detection bound for 100GeV DM, we should have

$$\sigma_{\chi N} < 10^{-45}\text{cm}^2 \times \frac{m_\chi}{100\text{GeV}},$$  

FIG. 4. Same as the right panel of Fig. 3 but with $m_\chi = 8\text{PeV}, \tau_\chi \sim 1.7 \times 10^{28}s$ (left), and $m_\chi = 10\text{PeV}, \tau_\chi \sim 1.5 \times 10^{28}s$ (right).
for heavy $m_\chi \sim 5$ PeV. This can be easily satisfied, for example, with $m_X \sim$ TeV and $\sin \epsilon \lesssim 0.1$.

V. RELIC ABUNDANCE AND CONSTRAINTS

In our above investigation, we have not discussed the relic abundance for DM $\chi$ yet. Since $\chi$ is very heavy, the unitary bound on its annihilation makes the DM $\chi$ impossible to be thermally produced and a non-thermal process is needed (see Ref. [62] for a recent review on such topics). Here, we discuss one possible non-thermal production mechanism for DM $\chi$ in our model. We assume that the dark Higgs $\phi$\textsuperscript{7} once shared a common temperature with SM particles and had a thermal distribution when its temperature $T$ was larger than $m_\chi$. Here we do not specify the mechanism how $\phi$ reached such a temperature; it could be due to reheating after inflation or some heavy particle decays.

In the thermal bath, $\chi$ could be produced through $\phi + \phi \rightarrow \chi + \bar{\chi}$, whose thermal cross section is given by

$$\langle \sigma v \rangle \sim \frac{1}{16\pi} \left( \frac{f^2}{m_N} \right)^2.$$  

Here we considered the $m_N \gg T$ case only. We can calculate the $\chi$'s yield, $Y_\chi \equiv n_{\chi+\bar{\chi}}/s$, where $s \sim g_s(T)T^3$ is the total entropy density in the Universe ($g_s(T) \sim 100$),

$$Y_\chi \sim n_{\phi} \langle \sigma v \rangle / \mathcal{H} \sim \frac{T \mathcal{M}_{pl} \langle \sigma v \rangle}{g_s(T) \sqrt{g_*(T)}}. \quad (5.1)$$

In the above derivation we have used the Hubble parameter $\mathcal{H} \simeq \sqrt{g_*(T)T^2/M_{pl}}$, $g_*(T) \sim 100$ is the total effective number of degree of freedom when $\phi$'s temperature is $T$ and Planck mass $M_{pl} = \sqrt{3/8\pi G} \simeq 4.2 \times 10^{18}$ GeV. Since the yield has a positive power dependence on temperature, $\chi$ is mostly produced at $\phi$'s highest temperature $T_{\phi}^{\text{max}}$,

$$Y_\chi \sim \langle \sigma v \rangle \times \frac{T_{\text{max}}^{\phi} M_{pl}}{g_*(T_{\text{max}}^{\phi}) \sqrt{g_*(T_{\text{max}}^{\phi})}}. \quad (5.2)$$

Requiring $\chi$ give the correct relic density, we have a relation

$$Y_\chi \sim 6 \times 10^{-10} \left( \frac{\Omega_\chi}{\Omega_b} \right) \left( \frac{\text{GeV}}{m_\chi} \right) \sim 3 \times 10^{-15} \left( \frac{\text{PeV}}{m_\chi} \right), \quad (5.3)$$

which puts a constraint on $f$ and $m_N$,

$$\left( \frac{f^2}{m_N} \right)^2 \simeq 1.5 \times 10^{-13} \left( \frac{\text{PeV}}{m_\chi} \right) \times \frac{g_*(T_{\text{max}}^{\phi}) \sqrt{g_*(T_{\text{max}}^{\phi})}}{T_{\text{max}}^{\phi} M_{pl}}. \quad (5.4)$$

When $m_N > T_{\text{max}}^{\phi} > m_\chi$ and $m_\chi \sim \text{PeV}$, we are able to give a lower bound for $f$

$$|f| \gtrsim 10^{-6}.$$  

\textsuperscript{7} It should be $\Phi$ precisely since at high temperature symmetries are not yet broken, but it will not affect our discussion.
One more thing we can infer from Eq. (2.11) and (5.4) is that in this production mechanism $y$ would be too small such that this right-hand neutrino $N$ can not be fully responsible for active neutrino mass and mixing angles. This is because, in order to explain the active neutrino mass, we should have

$$\frac{y^2 v_H^2}{m_N} \simeq 0.1\text{eV} \Rightarrow y \sim 10^{-5} \left(\frac{m_N}{\text{PeV}}\right)^{1/2},$$

(5.5)

which can not be satisfied simultaneously with Eq. (2.11) and (5.4). This is not a problem for this model since we can expect there are additional right-handed neutrinos $N_i$ and they can couple to $\bar{L}H$ with large $y_i$ but to $\bar{\chi}\Phi$ with tiny $f_i$, so that they are just responsible for active neutrino mass and mixing angle but not for DM $\chi$’s production.

DM direct detection can constrain DM-nucleon scattering cross section, whose value in our model is determined by the kinetic mixing parameter $\epsilon$, gauge coupling $g_X$ and the mass of $Z'$. For GeV-TeV DM, there is already plenty of viable parameter space to evade such a constraint, see Ref. [63] for example. For PeV DM, the constraint is even relaxed due to the low number density, see Eq. 4.9. Indirect detection from positron, anti-proton and $\gamma$ rays also constrain DM $\chi$’s decay lifetime, see Refs. [64–66] and references therein for example. We have checked that $\tau_\chi \sim 10^{28}$ sec is still allowed by all such constraints.

As an illustration, in Fig. 5 we show the expected gamma-ray flux from DM decay with $m_\chi \sim 5\text{PeV}$ and lifetime $\tau_\chi \sim 2 \times 10^{28}$ s. We have included the prompt gamma-rays and those from inverse compton scattering (ICS) of charged particles on CMB, starlight and dust-rescattered light. For extragalactic contribution, we have taken absorption factor into account. As we can easily see, the flux is well below the current constraints from Fermi-LAT [67] and KASCADE [68]. Our results are also consistent with the recent investigations about gamma-ray constraints on the lifetime of PeV DM in different scenarios [36, 69], $\tau_\chi \gtrsim 3 \times 10^{27}$.

VI. CONCLUSION

In this paper, we have proposed a dark matter (DM) model that can explain the IceCube PeV events in terms of DM decay. The model is based on an extra $U(1)_X$ dark gauge symmetry which is spontaneously broken by a dark Higgs field, $\Phi$. One crucial bridge between DM $\chi$ and standard model (SM) particles is established by heavy right-handed (RH) neutrino portal interactions. This heavy neutrino can induce DM decays into SM particles, including the light neutrinos.

The dominant decay channel of DM is the three-body final state with SM Higgs, dark Higgs, and neutrino ($\chi \rightarrow \phi + h + \nu$) (and other channels due to the Goldstone boson equivalence theorem), and not the usual two-body decays such as $\chi \rightarrow Z\nu, W^{\pm}\ell^\mp$, etc.. This is a unique feature of the present model based on $U(1)_X$ dark gauge symmetry and the RH neutrino portal interactions. We have calculated both total and differential decay width to evaluate the galactic and extragalactic neutrino fluxes. We have found that neutrino flux from these decay products can agree well with the IceCube spectrum. Together with an astrophysical flux for lower energy events, we are able to fit IceCube data around $100\text{ TeV} \sim 2\text{ PeV}$ if we assume DM mass is about $m_\chi \sim 5\text{PeV}$ and its lifetime is $\tau_\chi \sim 2 \times 10^{28}$ sec.
FIG. 5. The gamma-ray flux from DM decay with $m_\chi \sim 5$ PeV and lifetime $\tau_\chi \sim 2 \times 10^{28}$ s, confronted with constraints from Fermi-LAT [67] and KASCADE [68] data.

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APPENDIX

Here we show the complete differential decay width for $\chi \to h + \phi + \nu$. Throughout the calculation, we work in the rest frame of $\chi$, so $\chi$’s momentum is $(m_\chi, 0, 0, 0)$. For unpolarized $\chi$, we have

$$d\Gamma = \frac{1}{(2\pi)^3} \frac{1}{8m_\chi} \sum_{pol} |M|^2 dE_\nu dE_h = \frac{1}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2 E_\nu dE_\nu dE_h,$$

where we have used the averaged, squared matrix element,

$$\sum_{pol} |M|^2 = 2 \left( \frac{yf}{m_N} \right)^2 (m_\chi E_\nu - m_\nu^2) \simeq 2 \left( \frac{yf}{m_N} \right)^2 m_\chi E_\nu.$$
Then we get

$$\frac{d\Gamma}{dE_{\nu}} = \frac{E_{\nu}}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2 \int_{E_{h}^{\min}}^{E_{h}^{\max}} dE_{h}$$

$$= \frac{E_{\nu}}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2 \frac{(m_{\phi\nu})_{\max} - (m_{\phi\nu})_{\min}}{2m_{\chi}}$$

$$= \frac{2E_{\nu}}{(2\pi)^3 m_{\chi}} \left( \frac{yf}{2m_N} \right)^2 \sqrt{E_{\phi}^2 - m_{\phi}^2} \sqrt{E_{\nu}^2 - m_{\nu}^2}.$$

(6.2)

$$\simeq \frac{E_{\nu}^2}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2 \text{(with } E_{\nu} < m_{\chi}/2). \quad (6.3)$$

In the last line we have used the heavy $m_{\chi}$ limit, $m_{\chi} \gg m_{h}, m_{\chi} \gg m_{\phi\nu}$ and $m_{\nu} \simeq 0$. Some definitions are listed below,

$$E_{h} = \frac{m_{\chi}^2 + m_{h}^2 - m_{\phi\nu}^2}{2m_{\chi}},$$

$$m_{ab} = (p_{a} + p_{b})^2, m_{ab} = \sqrt{(p_{a} + p_{b})^2},$$

and some other kinematic variables,

$$(m_{\phi\nu})_{\max} = (E_{\phi}^* + E_{\nu}^*)^2 - \left( \sqrt{E_{\phi}^2 - m_{\phi}^2} - \sqrt{E_{\nu}^2 - m_{\nu}^2} \right)^2,$$

$$(m_{\phi\nu})_{\min} = (E_{\phi}^* + E_{\nu}^*)^2 - \left( \sqrt{E_{\phi}^2 - m_{\phi}^2} + \sqrt{E_{\nu}^2 - m_{\nu}^2} \right)^2,$$

$$E_{\phi}^* = \frac{m_{h\phi}^2 - m_{h}^2 + m_{\phi}^2}{2m_{h\phi}}, E_{\nu}^* = \frac{m_{\chi}^2 - m_{h\phi}^2 + m_{\nu}^2}{2m_{h\phi}},$$

$$m_{h\phi}^2 = m_{\chi}^2 + m_{\nu}^2 - 2m_{\chi}E_{\nu},$$

where $E_{\phi}^*$ and $E_{\nu}^*$ are the energies of $\phi$ and $\nu$ in the $m_{h\phi}$ rest frame, respectively. From the above differential decay width, we can easily get the total width

$$\Gamma \simeq \frac{1}{24} \frac{m_{\chi}^3}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2.$$

(6.4)

The differential decay width as function of $E_{h}$ or $E_{\phi}$ can also be calculated similarly. For example,

$$\frac{d\Gamma}{dE_{h}} = \frac{1}{(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2 \int_{E_{\nu}^{\min}}^{E_{\nu}^{\max}} E_{\nu} dE_{\nu}$$

$$= \frac{1}{2} \left( \frac{yf}{2m_N} \right)^2 \left[ (E_{\nu}^{\max})^2 - (E_{\nu}^{\min})^2 \right],$$

(6.5)

$$\simeq \frac{E_{h} (m_{\chi} - E_{h})}{2(2\pi)^3} \left( \frac{yf}{2m_N} \right)^2, E_{h} < m_{\chi}/2.$$
Again, in the second line we have used the massless limit. The neutrino energy $E_\nu$ in $\chi$'s rest frame can be written as

$$E_\nu = \frac{m_\chi^2 + m_\nu^2 - m_{\phi h}^2}{2m_\chi},$$

(6.7)

with similar definitions and kinematic bounds,

$$(m_{\phi h}^2)_{\text{max}} = (E_\phi^* + E_h^*)^2 - \left(\sqrt{E_\phi^{*2} - m_\phi^2} - \sqrt{E_h^{*2} - m_h^2}\right)^2,$$

$$(m_{\phi h}^2)_{\text{min}} = (E_\phi^* + E_h^*)^2 - \left(\sqrt{E_\phi^{*2} - m_\phi^2} + \sqrt{E_h^{*2} - m_h^2}\right)^2,$$

$$E_\phi^* = \frac{m_\phi^2 - m_\nu^2 + m_\phi^2}{2m_\phi^*}, E_h^* = \frac{m_\chi^2 - m_{\phi h}^2 + m_h^2}{2m_{\phi h}},$$

now here $E_\phi^*$ and $E_h^*$ are the energies of $\phi$ and $h$ in the $m_\phi$ rest frame, respectively.

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[1] **IceCube**, M. G. Aartsen et al., *Observation of High-Energy Astrophysical Neutrinos in Three Years of IceCube Data*, Phys. Rev. Lett. **113** (2014) 101101 [arXiv:1405.5303].

[2] **IceCube**, M. Aartsen et al., *First observation of PeV-energy neutrinos with IceCube*, Phys.Rev.Lett. **111** (2013) 021103 [arXiv:1304.5356].

[3] **IceCube**, M. G. Aartsen et al., *Evidence for High-Energy Extraterrestrial Neutrinos at the IceCube Detector*, Science **342** (2013) 1242856 [arXiv:1311.5238].

[4] **IceCube**, M. G. Aartsen et al., *Flavor Ratio of Astrophysical Neutrinos above 35 TeV in IceCube*, Phys. Rev. Lett. **114** no. 17, (2015) 171102 [arXiv:1502.03376].

[5] S. Palomares-Ruiz, A. C. Vincent, and O. Mena, *Spectral analysis of the high-energy IceCube neutrinos*, Phys. Rev. **D91** no. 10, (2015) 103008 [arXiv:1502.02649].

[6] M. Bustamante, J. F. Beacom, and W. Winter, *Theoretically palatable flavor combinations of astrophysical neutrinos*, [arXiv:1506.02645].

[7] Y. Huang and B.-Q. Ma, *Neutrino properties from ultra-high energy cosmic neutrinos*, [arXiv:1508.01698].

[8] S. Chakraborty and I. Izaguirre, *Diffuse neutrinos from extragalactic supernova remnants: Dominating the 100 TeV IceCube flux*, Phys. Lett. **B745** (2015) 35–39 [arXiv:1501.02615].

[9] A. Loeb and E. Waxman, *The cumulative background of high energy neutrinos from starburst galaxies*, JCAP **0605** (2006) 003 [astro-ph/0601695].

[10] K. Murase, M. Ahlers, and B. C. Lacki, *Testing the Hadronuclear Origin of PeV Neutrinos Observed with IceCube*, Phys. Rev. **D88** no. 12, (2013) 121301 [arXiv:1306.3417].

[11] X.-C. Chang, R.-Y. Liu, and X.-Y. Wang, *Star-forming galaxies as the origin of the IceCube PeV neutrinos*, Astrophys. J. **805** no. 2, (2015) 95 [arXiv:1412.8361].

[12] R.-Y. Liu, X.-Y. Wang, S. Inoue, R. Crocker, and F. Aharonian, *Diffuse PeV neutrinos from EeV cosmic ray sources: Semirelativistic hypernova remnants in star-forming galaxies*, Phys. Rev. **D89** no. 8, (2014) 083004 [arXiv:1310.1263].

[13] O. E. Kalashev, A. Kusenko, and W. Essey, *PeV neutrinos from intergalactic interactions of cosmic rays emitted by active galactic nuclei*, Phys.Rev.Lett. **111** no. 4, (2013) 041103 [arXiv:1303.0300].
[14] O. Kalashev, D. Semikoz, and I. Tkachev, *Neutrinos in IceCube from AGN’s*, [arXiv:1410.8124].
[15] F. W. Stecker, C. Done, M. H. Salamon, and P. Sommers, *High-energy neutrinos from active galactic nuclei*, Phys. Rev. Lett. 66 (1991) 2697–2700. [Erratum: Phys. Rev. Lett.69,2738(1992)].
[16] W. Essey, O. E. Kalashev, A. Kusenko, and J. F. Beacom, *Secondary photons and neutrinos from cosmic rays produced by distant blazars*, Phys. Rev. Lett. 104 (2010) 141102 [arXiv:0912.3976].
[17] E. Waxman and J. N. Bahcall, *High-energy neutrinos from cosmological gamma-ray burst fireballs*, Phys. Rev. Lett. 78 (1997) 2292–2295 [astro-ph/9701231].
[18] K. Murase and K. Ioka, *TeV–PeV Neutrinos from Low-Power Gamma-Ray Burst Jets inside Stars*, Phys. Rev. Lett. 111 no. 12, (2013) 121102 [arXiv:1306.2274].
[19] M. Ahlers and K. Murase, *Probing the Galactic Origin of the IceCube Excess with Gamma-Rays*, Phys. Rev. D90 no. 2, (2014) 023010 [arXiv:1309.4077].
[20] S. Razzaque, *The Galactic Center Origin of a Subset of IceCube Neutrino Events*, Phys. Rev. D88 (2013) 081302 [arXiv:1309.2756].
[21] B. Wang, X.-H. Zhao, and Z. Li, *Implications of Fermi-LAT observations on the origin of IceCube neutrinos*, JCAP 1411 no. 11, (2014) 028 [arXiv:1407.2536].
[22] M. Ahlers, Y. Bai, V. Barger, and R. Lu, *Galactic TeV-PeV Neutrinos*, [arXiv:1505.03156].
[23] B. Feldstein, A. Kusenko, S. Matsumoto, and T. T. Yanagida, *Neutrinos at IceCube from Heavy Decaying Dark Matter*, Phys.Rev. D88 no. 1, (2013) 015004 [arXiv:1303.7320].
[24] A. Esmaili and P. D. Serpico, *Are IceCube neutrinos unveiling PeV-scale decaying dark matter?*, JCAP 1311 (2013) 054 [arXiv:1308.1105].
[25] Y. Ema, R. Jinno, and T. Moroi, *Cosmic-Ray Neutrinos from the Decay of Long-Lived Particle and the Recent IceCube Result*, Phys. Lett. B733 (2014) 120–125 [arXiv:1312.3501].
[26] A. Esmaili, S. K. Kang, and P. D. Serpico, *IceCube events and decaying dark matter: hints and constraints*, JCAP 1412 no. 12, (2014) 054 [arXiv:1410.5979].
[27] Y. Ema, R. Jinno, and T. Moroi, *Cosmological Implications of High-Energy Neutrino Emission from the Decay of Long-Lived Particle*, JHEP 10 (2014) 150 [arXiv:1408.1745].
[28] C. S. Fong, H. Minakata, B. Panes, and R. Z. Funchal, *Possible Interpretations of IceCube High-Energy Neutrino Events*, JHEP 02 (2015) 189 [arXiv:1411.5318].
[29] T. Higaki, R. Kitano, and R. Sato, *Neutrinoful Universe*, JHEP 07 (2014) 044 [arXiv:1405.0013].
[30] A. Bhattacharya, M. H. Reno, and I. Sarcevic, *Reconciling neutrino flux from heavy dark matter decay and recent events at IceCube*, JHEP 06 (2014) 110 [arXiv:1403.1862].
[31] L. A. Anchordoqui, V. Barger, H. Goldberg, X. Huang, D. Marfatia, L. H. M. da Silva, and T. J. Weiler, *IceCube neutrinos, decaying dark matter, and the Hubble constant*, [arXiv:1506.08788].
[32] S. M. Boucenna, M. Chianese, G. Mangano, G. Miele, S. Morisi, O. Pisanti, and E. Vitagliano, *Decaying Leptophilic Dark Matter at IceCube*, [arXiv:1507.01000].
[33] C. E. Aisati, M. Gustafsson, and T. Hambly, *New Search for Monochromatic Neutrinos from Dark Matter Decay*, [arXiv:1506.02657].
[34] S. B. Roland, B. Shakya, and J. D. Wells, *PeV Neutrinos and a 3.5 keV X-Ray Line from a PeV Scale Supersymmetric Neutrino Sector*, [arXiv:1506.08195].
[35] C. Rott, K. Kohri, and S. C. Park, *Superheavy dark matter and IceCube neutrino
signals: bounds on decaying dark matter, [arXiv:1408.4575].

[36] K. Murase, R. Laha, S. Ando, and M. Ahlers, Testing the Dark Matter Scenario for PeV Neutrinos Observed in IceCube, [arXiv:1503.04663].

[37] Z. Berezhiani, Shadow dark matter, sterile neutrinos and neutrino events at IceCube, in Neutrino Oscillation Workshop (NOW 2014), Lecce, Italy, September 7-14, 2014. 2015 [arXiv:1506.09040].

[38] J. Zavala, Galactic PeV neutrinos from dark matter annihilation, Phys. Rev. D89 no. 12, (2014) 123516 [arXiv:1404.2932].

[39] A. Bhattacharyya, R. Gandhi, and A. Gupta, The Direct Detection of Boosted Dark Matter at High Energies and PeV events at IceCube, JCAP 1503 no. 03, (2015) 027 [arXiv:1407.3280].

[40] J. Kopp, J. Liu, and X.-P. Wang, Boosted Dark Matter in IceCube and at the Galactic Center, JHEP 04 (2015) 105 [arXiv:1503.02669].

[41] V. Barger and W.-Y. Keung, Superheavy Particle Origin of IceCube PeV Neutrino Events, Phys.Lett. B727 (2013) 190–193 [arXiv:1305.6907].

[42] H.-N. He, R.-Z. Yang, Y.-Z. Fan, and D.-M. Wei, TeV-PeV neutrinos over the atmospheric background: originating from two groups of sources?, [arXiv:1307.1450].

[43] K. Ioka and K. Murase, IceCube PeVNeV neutrinos and secret interactions of neutrinos, PTEP 2014 no. 6, (2014) 061E01 [arXiv:1404.2279].

[44] T. Araki, F. Kaneko, Y. Konishi, T. Ota, J. Sato, and T. Shimomura, Cosmic neutrino spectrum and the muon anomalous magnetic moment in the gauged $L_\mu - L_\tau$ model, Phys. Rev. D91 no. 3, (2015) 037301 [arXiv:1409.4180].

[45] J. F. Cherry, A. Friedland, and I. M. Shoemaker, Neutrino Portal Dark Matter: From Dwarf Galaxies to IceCube, [arXiv:1411.1071].

[46] C.-Y. Chen, P. S. B. Dev, and A. Soni, A Possible Two-component Flux for the High Energy Neutrino Events at IceCube, [arXiv:1411.5658].

[47] A. Kamada and H.-B. Yu, Coherent Propagation of PeV Neutrinos and the Dip in the Neutrino Spectrum at IceCube, [arXiv:1504.00711].

[48] P. Ko and Y. Tang, AMS02 positron excess from decaying fermion DM with local dark gauge symmetry, Phys. Lett. B741 (2015) 284–289 [arXiv:1410.7657].

[49] Z. Kang and T. Li, Decaying Dark Matter in the Supersymmetric Standard Model with Freeze-in and Seesaw mechanisms, JHEP 02 (2011) 035 [arXiv:1008.1621].

[50] Y. Tang, Vacuum Stability in the Standard Model, Mod.Phys.Lett. A28 (2013) 1330002 [arXiv:1301.5812].

[51] C.-S. Chen and Y. Tang, Vacuum stability, neutrinos, and dark matter, JHEP 04 (2012) 019 [arXiv:1202.5717].

[52] S. Baek, P. Ko, W.-I. Park, and E. Senaha, Vacuum structure and stability of a singlet fermion dark matter model with a singlet scalar messenger, JHEP 11 (2012) 116 [arXiv:1209.4163].

[53] S. Baek, P. Ko, W.-I. Park, and E. Senaha, Higgs Portal Vector Dark Matter : Revisited, JHEP 1305 (2013) 036 [arXiv:1212.2131].

[54] S. Baek, P. Ko, W.-I. Park, and Y. Tang, Indirect and direct signatures of Higgs portal decaying vector dark matter for positron excess in cosmic rays, JCAP 1406 (2014) 046 [arXiv:1402.2115].

[55] G. ’t Hooft, Naturalness, chiral symmetry, and spontaneous chiral symmetry breaking, NATO Sci. Ser. B 59 (1980) 135.
[56] J. F. Navarro, C. S. Frenk, and S. D. M. White, *The Structure of cold dark matter halos*, Astrophys. J. **462** (1996) 563–575 [astro-ph/9508025].

[57] Planck Collaboration, P. Ade et al., *Planck 2015 results. XIII. Cosmological parameters*, [arXiv:1502.01589].

[58] T. Sjostrand, S. Mrenna, and P. Z. Skands, *PYTHIA 6.4 Physics and Manual*, JHEP **05** (2006) 026 [hep-ph/0603175].

[59] M. Cirelli, G. Corcella, A. Hektor, G. Hutsi, M. Kadastik, P. Panci, M. Raidal, F. Sala, and A. Strumia, *PPPC 4 DM ID: A Poor Particle Physicist Cookbook for Dark Matter Indirect Detection*, JCAP **1103** (2011) 051 [arXiv:1012.4515]. [Erratum: JCAP1210,E01(2012)].

[60] IceCube, M. G. Aartsen et al., *A combined maximum-likelihood analysis of the high-energy astrophysical neutrino flux measured with IceCube*, Astrophys. J. **809** no. 1, (2015) 98 [arXiv:1507.03991].

[61] C. Kopper, *Neutrino Astronomy*, [34th International Cosmic Ray Conference].

[62] H. Baer, K.-Y. Choi, J. E. Kim, and L. Roszkowski, *Dark matter production in the early Universe: beyond the thermal WIMP paradigm*, Phys. Rept. **555** (2014) 1–60 [arXiv:1407.0017].

[63] P. Ko and Y. Tang, *Self-interacting scalar dark matter with local Z3 symmetry*, JCAP **1405** (2014) 047 [arXiv:1402.6449].

[64] A. Esmaili, A. Ibarra, and O. L. G. Peres, *Probing the stability of superheavy dark matter particles with high-energy neutrinos*, JCAP **1211** (2012) 034 [arXiv:1205.5281].

[65] K. Murase and J. F. Beacom, *Constraining Very Heavy Dark Matter Using Diffuse Backgrounds of Neutrinos and Cascaded Gamma Rays*, JCAP **1210** (2012) 043 [arXiv:1206.2595].

[66] A. Ibarra, D. Tran, and C. Weniger, *Indirect Searches for Decaying Dark Matter*, Int. J. Mod. Phys. **A28** (2013) 1330040 [arXiv:1307.6434].

[67] Fermi-LAT, M. Ackermann et al., *The spectrum of isotropic diffuse gamma-ray emission between 100 MeV and 820 GeV*, Astrophys. J. **799** no. 1, (2015) 86 [arXiv:1410.3696].

[68] G. Schatz et al., *Search for extremely high energy gamma rays with the KASCADE experiment*, in Proceedings, 28th International Cosmic Ray Conference (ICRC 2003), pp. 2293–2296. 2003. http://www-rccn.icrr.u-tokyo.ac.jp/icrc2003/PROCEEDINGS/PDF/566.pdf.

[69] A. Esmaili and P. D. Serpico, *Gamma-ray bounds from EAS detectors and heavy decaying dark matter constraints*, [arXiv:1505.06486].

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