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To cite this article: J C D'Olive et al 2006 J. Phys.: Conf. Ser. 39 422

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Thermal effects on the absorption of ultra-high energy neutrinos by the cosmic neutrino background

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Abstract. We use the formalism of finite-temperature field theory to study the interactions of ultra-high energy (UHE) cosmic neutrinos with the background of relic neutrinos and to derive general expressions for the UHE neutrino transmission probability. This approach allows us to take into account the thermal effects introduced by the momentum distribution of the relic neutrinos. We compare our results with the approximate expressions existing in the literature and discuss the influence of thermal effects on the absorption dips in the context of favoured neutrino mass schemes, as well as in the case of clustered relic neutrinos.

1. Introduction

The interaction of cosmic neutrinos at ultra-high energies (UHEν) with the cosmological background of relic (anti) neutrinos (CνB) has been proposed as an indirect way of observing the CνB [1]. Provided adequate sensitivity and energy resolution of the detectors, the observation in the UHEν flux of absorption lines associated with the resonant production of a Z boson (νν → Z → f̅f) could allow the determination of the absolute neutrino masses [2]. The shape and depth of these absorption dips may also reflect features of the distribution of UHEν sources and their emission spectrum [3, 4]. Most of the work in the literature describe the UHEν-CνB interactions assuming that relic neutrinos are at rest. The effects of thermal motion in the CνB (whose present temperature is ≈ 1.69 × 10^{-4} eV), however, become relevant as soon as the momentum of the relic neutrinos gets comparable to their mass. In this work, we take into account the thermal effects on the dominant (resonant) contribution to the neutrino damping by using finite-temperature field theory (FTFT) [5]. In section 2 we present the UHEν transmission probability across the CνB for various mass schemes, and in section 3 we briefly discuss the impact of thermal motion on the absorption in relic neutrino clusters.

2. Transmission probability of UHEν across the CνB

For an UHEν with four-momentum \( k^\mu = (E_K, \vec{K}) \) and mass \( m_\nu \) travelling across the CνB, the equation of motion reads \( (k - m_\nu - \Sigma) \psi = 0 \). The self-energy \( \Sigma \) embodies the effects of the surrounding neutrino medium, coming in this case from the exchange of a Z boson. The corresponding dispersion relation is given by \( \mathcal{E}_K = \mathcal{E}_r - i\frac{\gamma}{2} \), where \( \mathcal{E}_r \) and \( \gamma \) are functions of \( K \). In the real-time formalism of FTFT, one calculates \( \Sigma \) from the corresponding Feynman diagram, having in mind that the vertices are doubled respect to the standard theory, and that the propagators of the Z boson (near the resonance) and of the relic neutrino become 2 × 2 matrices.
The relic neutrino propagator also depend on the functions $f_\nu(P)$ and $f_\bar{\nu}(P)$ characterizing the momentum distribution of (anti) neutrinos in the thermal bath. These functions take the simple relativistic Fermi-Dirac form $f_\nu(P) = f_\bar{\nu}(P) = 1/(e^{P/T_\nu} + 1)$, where $T_\nu$ is the temperature of the C$\nu$B and we have neglected the chemical potential.

The damping factor $\gamma_\nu$, which governs the attenuation of the UHE$\nu$ flux across the background of relic neutrinos, is directly related to the imaginary part of the self-energy $\Sigma_i$ with an energy $K$.

According to recent calculations [8], depending on their mass and on the properties of the dark matter distribution, relic neutrinos cluster on scales ranging from $10^{-1}$ to 1 Mpc with overdensity factors $N_{cd}$ of the order of $10^{-4}$ with respect to the present background density ($n_\nu \approx 56 \text{cm}^{-3}$).

### 3. Absorption lines due to relic neutrino clustering

According to recent calculations [8], depending on their mass and on the properties of the dark matter distribution, relic neutrinos cluster on scales ranging from $0.01$ to 1 Mpc with overdensity factors $N_{cd}$ of the order of $10 - 10^4$ with respect to the present background density ($n_\nu \approx 56 \text{cm}^{-3}$).
respectively. The right plots assume an inverted hierarchy with masses \(5 \times 10^{-z} \text{ eV}\) for a source located at redshifts \(z_s = 5, 10, 20\) (from top to bottom in each plot). The two left plots assume a normal hierarchy for the \(m_{\nu}\), with values \((5 \times 10^{-2} \text{ eV}, 9 \times 10^{-3} \text{ eV}, 10^{-3} \text{ eV})\) and \((5 \times 10^{-2} \text{ eV}, 9 \times 10^{-3} \text{ eV}, 10^{-4} \text{ eV})\) respectively. The right plots assume an inverted hierarchy with masses \((5 \times 10^{-2} \text{ eV}, 5 \times 10^{-2} \text{ eV}, 10^{-3} \text{ eV})\) and \((5 \times 10^{-2} \text{ eV}, 5 \times 10^{-2} \text{ eV}, 10^{-4} \text{ eV})\) respectively. The continued, black curves correspond to the full damping as from eq. (1) and (2), while the dotted (red) curves are for the approximation of relic neutrinos at rest.

Figure 2. Transmission probability for a cluster of extension 1 Mpc, made of neutrinos of mass 1 eV (left) and \(10^{-1} \text{ eV}\) (right), with a constant neutrino density \(n_{\nu}^{cl} = 10^3 n_{0\nu}\) and \(n_{\nu}^{cl} = 10^4 n_{0\nu}\) (from top to bottom in each plot). The colour code is the same as in fig. 1.

per species). To compute the UHE\(\nu\) absorption by clustered neutrinos we replaced \(f_{\nu}(P)\) in eq. 1 by a modified Fermi-Dirac distribution,

\[
f_{\nu}^{cl}(P) = \frac{1}{2} \frac{e^{-\Phi/T_{\nu}} + 1}{e^{(P-\Phi)/T_{\nu}} + 1},
\]

which fits reasonably well the profiles obtained in numerical calculations using Vlasov equation [8]. For a given overdensity factor \(N_{cl}\) we solve \(\int_{0}^{\infty} \frac{dP}{2\pi} P^2 f_{\nu}^{cl}(P) = N_{cl} n_{0\nu}\) for \(\Phi\). We computed the UHE\(\nu\) transmission probability across a cluster located between the UHE\(\nu\) source and the observer and found that the effect of the thermal motion of relic neutrinos is in general small or negligible. This is essentially because clustering is efficient only for neutrinos with mass \(m_{\nu} \gtrsim 0.1 \text{ eV}\), and because it is achieved only at small redshifts, when the CMB temperature is still very small. As shown in fig. 2, we have to saturate the bounds on the parameters to obtain a significant effect. For a maximal overdensity factor \(N_{cl} = 10^4\), thermal effects reduce the maximum absorption probability across the cluster from \(\approx 55\%\) to \(\approx 35\%\).

Acknowledgments
We would like to acknowledge support by CONACyT under grants 34868-E and 46999-F and by DGAPA-UNAM under grants PAPIIT IN116503, IN119405, and IN112105.

References
[1] Weiler T J 1982 Phys. Rev. Lett. 49 234
[2] Pas H and Weiler T J 2001 Phys. Rev. D 63 113015
[3] Eberle B, Ringwald A, Song L, and Weiler T J 2004 Phys. Rev. D 70 023007
[4] Barenboim G, Mena Requejo O and Quigg C 2005 *Phys. Rev.* D **71** 083002
[5] D’Olivo J C, Nellen L, Sahu S and Van Elewyck V 2005 *Preprint* astro-ph/0507333
[6] D’Olivo J F and Nieves J F 1995 *Phys. Rev.* D **52** 2987
[7] Beacom J F and Bell N F 2002 *Phys. Rev.* D **65** 113009
[8] Ringwald A and Wong Y Y Y 2004 *JCAP* **0412** 005