The interpretation of water emission from dense interstellar clouds
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ABSTRACT

Context. Existing SWAS observations and future HIFI/Herschel data require a clear sense of the information content of water emission and absorption lines.

Aims. Investigate whether the ground-state transition of ortho-H$_2$O (1$_{10}$→1$_{01}$) at 557 GHz can be used to measure the column density throughout an interstellar cloud.

Methods. We make use of a multi-zone escape probability code suitable for the treatment of molecular line emission.

Results. For low abundances, i.e., X(H$_2$O) ≤ 10$^{-8}$, the intensity of the 1$_{10}$→1$_{01}$ transition scales with the total column of H$_2$. However, this relationship breaks down with increasing abundance, i.e., optical depth, due to line trapping and, – for T$_{dust}$ ≥ 25 K, X(H$_2$O) ≤ 10$^{-8}$ and $~$10$^{-9}$ cm$^{-3}$, – absorption of the dust continuum.

Conclusions. An observed decline in intensity per column, expected if H$_2$O is a surface tracer, does not necessarily mean that the water is absent in the gas phase at large columns, but can be caused by line trapping and subsequent collisional de-excitation. To determine the amount of water vapour in the interstellar medium, multiple line measurements of optically thin transitions are needed to disentangle radiative transfer and local excitation effects.

Key words. ISM: molecules – radiative transfer

1. Introduction

The launch of the Submillimeter Wave Astronomy Satellite (SWAS; Melnick et al. 2000) made it possible to observe emission from the ground-state transition (1$_{10}$→1$_{01}$) of ortho-H$_2$O and its isotopomer ortho-H$_2^{18}$O, to determine the abundance of water vapour, i.e., column density N$_{H_2O}$ in various regions in the interstellar medium, e.g., dense and diffuse interstellar gas clouds, circumstellar envelopes, planetary atmospheres, and comets (e.g., Melnick et al. 2000, Snell et al. 2000a,b; Encrenaz et al. 1995; Bergin et al. 2000a; Gurwell et al. 2000, Melnick et al. 2000). In the future, the Heterodyne Instrument for the Far Infrared (HIFI) on Herschel will observe even more transitions of ortho- and para-H$_2$O (o/p-H$_2$O) like 2$_{12}$→1$_{10}$ (1669.904 GHz), 2$_{12}$→2$_{11}$ (1661.015 GHz), 3$_{12}$→2$_{12}$ (1716.774 GHz), 3$_{12}$→3$_{03}$ (1097.357 GHz), 3$_{21}$→3$_{12}$ (1162.910 GHz), 1$_{11}$→0$_{00}$ (1113.342 GHz), 2$_{02}$→1$_{11}$ (967.924 GHz), 2$_{11}$→2$_{02}$ (752.029 GHz) and 2$_{20}$→2$_{11}$ (1228.801 GHz); some in absorption while others in emission.

One of the main goals of the SWAS mission is to determine where and whether H$_2$O and O$_2$ are the major reservoirs of oxygen through the interstellar medium. SWAS observations have determined the gaseous water abundance in warm dense gas (T ≥ 300 K and n(H$_2$) ≥ 10$^7$ cm$^{-3}$) to be 10$^{-5}$ relative to H$_2$, in good agreement with chemical models for similar conditions. However, in cold (T ≤ 30 K), dense clouds the abundance of gaseous water is ~100 to 1000 times below the predictions of cold-cloud gas-phase chemical models. It has been suggested that – toward cold clouds – gaseous H$_2$O exists only near the cloud surface. Indeed, closer to the surface than an AV of a few mag, H$_2$O is photo-dissociated by the ambient galactic UV field. Deeper into the cloud, i.e., AV of 4 ~8 mag (depending on density and UV intensity), H$_2$O may rapidly deplete onto dust grains (Bergin et al. 2000, Charney et al. 2001, Viti et al. 2001). Although the derivation of the column density from absorption observations is straightforward (column density is simply proportional to the optical depth in the line, see Plume et al. 2004) this is not the case for emission observations. The analysis to determine the H$_2$O abundance now crucially depends on the physical properties of the gas through the collisional rate coefficients. Therefore, accurate constraints on the gas densities and temperatures are needed.

Extensive SWAS observations of the Orion A molecular cloud show that gaseous H$_2$O correlates with CN, a surface tracer, rather than with C$^{18}$O, a volume tracer (Melnick & Bergin 2005). This result has been interpreted as evidence that gaseous water resides only near the surface. However, caution is needed when relying purely on single transition observations to draw such a conclusion in view of the complex rotational level structure of the H$_2$O molecule. In particular, there is a fundamental difference between an optically thin and an effectively optically thin line. The latter case implies a strong coupling between line photons and water molecules. A full radiative transfer calculation is needed to address this problem, since the observed intensities of molecular emission depend on a complex competition between radiative and collisional processes. Moreover, the excitation of H$_2$O also differs from that of other molecules, since both collisions and infrared radiation from warm dust influence the level populations (Takahashi et al. 1983).

The intent of this work is to show that it is not straightforward to retrieve accurate information, e.g., column density, from single
transition observations of H$_2$O due to the complex level structure of this molecule.

2. Basic model description

The results presented here were obtained by application of the numerical code of [Poelman & Spaans (2005)], described further in [Poelman & Spaans (2006)]. The interested reader is referred to these papers for a description of the underlying algorithms. The radiative transfer of o/p-H$_2$O is solved by means of a multi-zone escape probability method in three dimensions. By using a multi-zone formalism, the medium is divided into different zones, i.e., grid cells, each with a value for the abundance of the species (e.g., H$_2$O), the density of the medium, and the temperature of gas and dust. Besides this, the cloud is characterized by a fixed total column density. The statistical equilibrium equation for a multi-level system can be written as

$$\sum_{i>j}(n_iA_{ij} + n_n\gamma_{ij} + n_jB_{ji}) = \sum_{i<j}(n_n\gamma_{ij} + n_iB_{ij}),$$

(1)

where the radiative de-excitation is given by the Einstein A coefficients, $B_j$ are the Einstein coefficients for absorption and stimulated emission, $\gamma_{ij}$ are the collisional rate coefficients, $J$ the mean photon radiation field, $n_i$ the population density of the $i$th level, and $n$ the density of the medium. The level populations depend on the radiation field while the radiation field depends on the level populations everywhere. By introducing the concept of a multi-zone escape probability [Poelman & Spaans (2005, 2006)] the statistical equilibrium equations are decoupled from the radiative transfer equations. Eq. [1] can be rewritten as

$$\sum_{i>j}(n_iA_{ij} + n_n\gamma_{ij}) = \sum_{i<j}(n_n\gamma_{ij}),$$

(2)

because the net absorptions, corrected for stimulated emission, are equal to those photons that do not escape, i.e.,

$$(n_iB_{ji} - n_jB_{ji})\sum_{i>j} = \sum_{i>j}n_i[1 - \beta(\tau_{ij})]A_{ij},$$

(3)

where $\beta(\tau)$ is the probability that a photon formed at optical depth $\tau$ in a certain direction escapes the cloud along that direction. Therefore,

$$n_{cr} = \frac{\sum_{i>j}\beta(\tau_{ij})A_{ij}}{\sum_{i<j}\gamma_{ij}}$$

(4)

Note that because of the large Einstein A coefficients of the water molecule critical densities are of the order of $10^8$-10$^9$ cm$^{-3}$ in the optically thin case.

The background radiation field $P(v_{ij})$ in the code consists of two terms: the 2.7K microwave background and the infrared emission of dust at a temperature $T_d$. This is,

$$P(v_{ij}) = B(v_{ij}, T = 2.7K) + (1 - e^{-\tau_{dust}})B(v_{ij}, T_d)$$

(5)

The intensity of transition $i \rightarrow j$ ($i>j$) is then given by

$$I_{ij, total} = \frac{1}{4\pi} \int_0^{\tau} N_{i,j, local} dr,$$

(6)

with

$$N_{i,j, local} = n_i A_{ij} \hbar \nu_i \beta(\tau_{ij})[S(v_{ij}) - P(v_{ij})]/S(v_{ij}),$$

(7)

$S(v_{ij})$ is the source function at frequency $v_{ij}$.

Collisional rate coefficients for inelastic collisions between o/p-H$_2$O and He [Green et al. (1993)], and for collisions between o/p-H$_2$O and both o-H$_2$ and p-H$_2$ [Phillips et al. (1996)] are adopted. We adopt the expression for the ortho-to-para ratio (OPR) of H$_2$, in thermal equilibrium, defined by

$$\text{OPR} = \frac{(2I_o + 1)\sum(2J + 1)\exp(-\frac{E(J+1)K_o}{kT})}{(2I_p + 1)\sum(2J + 1)\exp(-\frac{E(J+1)K_p}{kT})},$$

(8)

where $I_o$ and $I_p$ are the total nuclear spin, corresponding to the wether the hydrogen nuclear spins are parallel ($I_o = 1, I_p \uparrow \uparrow$) or anti-parallel ($I_o = 0, I_p \uparrow \downarrow$). The sum in the numerator (denominator) extends over all ortho (para) levels ($\langle J, K_o, K_p \rangle$) [Mumma et al. (1987)]. The code has been tested extensively against (analytical) benchmark problems presented at the radiative transfer workshop held in Leiden (2004), see Poelman & Spaans (2006). It is found that the level populations are completely consistent with the solutions of other Monte Carlo and ALI codes, as presented in van der Tak et al. (2005).

### Table 1. Model parameters

| Model | n(H$_2$) | size [pc] | X(H$_2$O) | N(H$_2$) | T$_{gas}$ | T$_{dust}$ |
|-------|----------|-----------|-----------|----------|----------|-----------|
| I     | 10$^{-9}$ | 0.002-0.2 | 10$^{-1}$ | 10$^{-6}$ | 6x10$^{21}$ | 50 | no |
| II    | 10$^{-9}$ | 0.002-0.2 | 10$^{-1}$ | 10$^{-6}$ | 6x10$^{21}$ | 50 | 15 |
| III   | 10$^{-9}$ | 0.002-0.2 | 10$^{-1}$ | 10$^{-6}$ | 6x10$^{21}$ | 50 | 25 |
| IV    | 10$^{-9}$ | 0.002-0.2 | 10$^{-1}$ | 10$^{-6}$ | 6x10$^{21}$ | 50 | 50 |
| V     | 10$^{-9}$ | 0.002-0.2 | 10$^{-1}$ | 10$^{-6}$ | 6x10$^{21}$ | 30 | 15 |

$^a$ Abundance of H$_2$O; $^b$ Total column density through the centre.
cloud at the frequency of the ground state transition of o-H$_2$O, i.e., $\tau_{219}$=556.936GHz or $\tau_{3.6}$=539$\mu$m, is $10^{-3}$. Within each model the water abundance, $X$(H$_2$O), ranges from $10^{-10}$ to $10^{-6}$. The parameters for the different models are shown in Table I. Throughout the models, a velocity dispersion of 1 km s$^{-1}$ is adopted, typical for a cloud with moderate turbulence. Note that the results presented in this paper depend on the adopted velocity dispersion.

Fig. 1. The intensity of the ortho-H$_2$O ground state transition for a homogeneous sphere with H$_2$ densities of $10^4$(top), $10^5$(middle), $10^6$(bottom) cm$^{-3}$ and temperature of the gas of 50 K. The dust emission as well as the CMB radiation are ignored (i.e., model I). In every case, the total column density (H$_2$) is kept constant. Lines are plotted for an abundance of H$_2$O relative to H$_2$, from $10^{-10}$ (upper line/red) to $10^{-6}$ (lower line/light blue) as function of H$_2$ column density along the line of sight, where 2 x $10^{19}$ cm$^{-2}$ is at the edge, and 6 x $10^{21}$ cm$^{-2}$ through the center of the cloud. Y-axis in units of erg s$^{-1}$ sr$^{-1}$. The position of the $\tau=1$ surface is displayed with a cross for $X$(H$_2$O)=$10^{-9}$-$10^{-6}$.

Fig. 2. The intensity of the ortho-H$_2$O ground state transition for a homogeneous sphere with density (H$_2$) of $10^4$ cm$^{-3}$ for model II (top), III (middle) and IV (bottom). Lines are plotted for an abundance of H$_2$O relative to H$_2$, from $10^{-10}$ (upper line/red) to $10^{-6}$ (lower line/light blue) as function of H$_2$ column density along the line of sight, where 2 x $10^{19}$ cm$^{-2}$ is at the edge, and 6 x $10^{21}$ cm$^{-2}$ through the center of the cloud. Y-axis in units of erg s$^{-1}$ sr$^{-1}$.

Fig. 3. The intensity of the ortho-H$_2$O ground state transition in case of a homogeneous sphere with densities (H$_2$) of $10^4$(top), $10^5$(middle), $10^6$(bottom) cm$^{-3}$ and temperatures for gas and dust of 30 K and 15 K, respectively (i.e., model V). In every case, the total column density (H$_2$) is kept constant. Lines are plotted for an abundance of H$_2$O, relative to H$_2$, from $10^{-10}$ (upper line/red) to $10^{-6}$ (lower line/light blue) as function of H$_2$ column density along the line of sight, where 2 x $10^{19}$ cm$^{-2}$ is at the edge, and 6 x $10^{21}$ cm$^{-2}$ through the center of the cloud. Y-axis in units of erg s$^{-1}$ sr$^{-1}$.

Fig. 4. Shown here is the population of the $1_{01}$ level of o-H$_2$O as function of radius. Top, middle, bottom panel are the results in case $X$(H$_2$O) = $10^{-10}$, $10^{-9}$, $10^{-8}$, respectively. Dashed, dotted and dashed-dotted lines represent the results of model I, III and IV, respectively.

A higher (lower) velocity dispersion will decrease (increase) the optical depth for a given transition, hence having an impact on the excitation of the molecule.

Fig. 1, 2, 3, 4 present the basic results of this work. We plot, as a function of N(H$_2$), i.e., different impact parameter, the $1_{00}$→$1_{01}$ line intensity above the continuum per unit column density of o-H$_2$O, see Eq. [6]. The results for model I, in which we ignore the contribution of dust and CMB on the excitation of the water molecule are displayed in Fig. 1. The position of the $\tau=1$ surface is denoted by a cross for $X$(H$_2$O)=$10^{-9}$-$10^{-6}$. Models II, III and IV behave in a similar way as in model I in the case n(H$_2$)$\geq$10$^{17}$cm$^{-3}$.
For this reason, we only plot the outcome in the low density case for models II, III and IV in Fig. 2. The results for model V are plotted in Fig. 3.

The following trends can be identified, which will be discussed in Sect. 4.

First, in the case of \( n(\text{H}_2) \geq 10^5 \text{ cm}^{-3} \) and \( X(\text{H}_2O) \lesssim 10^{-8} \), i.e., \( \tau \ll 1 \), a linear relationship holds between the number of photons escaping the cloud and the impact parameter, i.e., \( I/N_{\text{H}_2O} \) is constant. However, this relationship breaks down at high optical depth, i.e., \( \text{H}_2O > 10 \), for all the models. Second, in all the models, except in model I, absorption occurs in the low density case when abundances are low, i.e., \( X(\text{H}_2O) < 10^{-8} \), which becomes more apparent as the dust temperature increases. However, the amount of absorption is moderate as the self-reversal in the center of the line is small. Third, when the \( \text{H}_2O \) abundance exceeds \( 10^{-7} \), in all the models, the ratio of the intensity to the column density decreases near the edge of the cloud (\( N(\text{H}_2) \sim 5 \times 10^{20} \text{ cm}^{-2} \)). Fourth, for high optical depth, i.e., \( X(\text{H}_2O) \geq 10^{-7} \), and \( n(\text{H}_2) = 10^6 \text{ cm}^{-3} \), \( I/N_{\text{H}_2O} \) decreases with increasing column density. Fifth, lowering the gas and dust temperatures by a factor of \( \sim 2 \) (model V) does not lead to significant differences in the shapes of the curves. That is, models II-IV and model V experience similar complicating radiative transfer effects.

4. Discussion

The asymmetry of the water molecule causes the rotational levels to split into a number of different ladders, so called ‘K-ladders’, characterized by different values of the projection of the angular momentum onto the principal axes of the molecule \( J_{K,K} \). Radiative transitions occur rapidly between levels in each ladder but are much slower between levels in different ladders. This leads to a spectrum more complex than linear or symmetric top molecules, e.g., CO, NH\(_3\). Hence, it is not straightforward to disentangle the different processes that contribute to the observed spectrum. We now describe the different effects that play a role in the interpretation of the figures. In this, the ‘edge’ and ‘centre’ of the cloud refers to an impact parameter of 1 and 0, respectively. Note that the use of spherical models leads to an-

![Fig. 5](image-url). Conversion of the results of model I (top) and IV (bottom) into surface area weighted values. In each panel the dashed-dotted, dotted, and dashed curve represent the results in case the density \( n(\text{H}_2) \) is \( 10^5 \), \( 10^4 \) and \( 10^3 \text{ cm}^{-3} \), respectively. Y-axis in units of erg s\(^{-1}\) sr\(^{-1}\).
tribution of the level populations and thus the absolute intensity in the lines. Hence, temperature variations cannot dispense of the radiative transfer effects studied in this work.
To summarize, we plot in Fig. 5 as a function of abundance, the average intensity emanating from the cloud for model I and IV, i.e.,
\[ \frac{\int I_{\text{H}_2O} \rightarrow \text{H}_2O(b)2\pi b \, db}{\int N_{\text{H}_2O}(b)2\pi b \, db} \]
with b the impact parameter. One notices a drop by a factor of \( \sim 2–5 \) in case \( n(\text{H}_2) \) is \( 10^3–10^6 \) cm\(^{-3} \), respectively. Note that with the assumption of an effectively optically thin line one would underestimate the water column by these same factors.

5. Astrophysical implications
The intensity of the ground-state transition of \( \text{o-H}_2\text{O} \) is driven by a combination of the ambient gas and dust temperatures on the one side and by the density of the surrounding medium on the other side. It is this interplay, together with the complex structure of the molecule that drives the level populations. To interpret existing SWAS and future HIFI data a clear sense of the information content of the water lines is needed.
SWAS observations of the lowest rotational transition of \( \text{o-H}_2\text{O} \) of the Orion A molecular cloud show that gaseous water correlates much better with the near surface tracer CN than with the volume tracer \( \text{C}^{18}\text{O} \), as presented in Melnick & Bergin (2005).
Through these observations – in which it is assumed that the ground-state transition of ortho-\( \text{H}_2\text{O} \) is effectively optically thin – one concludes that water is a surface tracer. This is plausible from a chemical point of view in which photo-dissociation destroys the water molecule near the surface. Further inwards the cloud the water abundance reaches its equilibrium value through photodesorption of \( \text{H}_2\text{O} \)-ice and photodestruction of \( \text{H}_2\text{O} \)-gas until it freezes-out onto dust grains deeper into the cloud. However, we have shown, as seen in Fig. 5 that for \( \tau>10 \) and \( n>10^5 \text{cm}^{-3} \) the effectively optically thin assumption no longer holds. Hence, under these conditions one is limited to observing the \( *\tau=10 * \) surface and cannot use water to trace the cloud’s volume, even when it is present, i.e., not frozen out (Cernicharo, private communication). Therefore, as CN is a surface tracer and the water intensity originates from a layer of gas with an optical thickness of 1 – depending on local excitation conditions this layer is a surface layer – the CN intensity correlates much better with the \( \text{H}_2\text{O} \) intensity and not with the volume tracer \( \text{C}^{18}\text{O} \). Thus, the anti-correlation of \( \text{H}_2\text{O} \) with \( \text{C}^{18}\text{O} \) is partly due to optical depth effects, and is not necessarily a result of chemical changes. As a consequence, the presence of water past the \( \tau=1 \) surface cannot be ruled out.
We would also like to point out here that the most interesting aspect of the correlation of the water line intensity with the CN line intensity is the fact that both are observed to vary by a factor \( \sim 100 \). Theoretically, the CN abundance is expected to scale with density squared (Boger & Sternberg 2005), indicating the importance of density variations over the Orion molecular cloud.
Given the results presented in this paper, we surmise that these density variations will hamper the interpretation of the water observations.
In order to deduce the total water column along the line of sight, additional information is needed from other – effectively optically thin – lines, which will be observed with future missions such as Herschel/HIFI.

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