High Fill Factors of Si Solar Cells Achieved by Using an Inverse Connection Between MOS and PN Junctions

Liang-Xing Wang1,2, Zhi-Quan Zhou1, Tian-Ning Zhang3, Xin Chen3 and Ming Lu1*

Abstract
Fill factors (FFs) of ~0.87 have been obtained for crystalline Si (c-Si) solar cells based on Ag front contacts after rapid thermal annealing. The usual single PN junction model fails to explain the high FF result. A metal/oxide/semiconductor (MOS) junction at the emitter is found to be inversely connected to the PN one, and when its barrier height $e$ is close to the open-circuit voltage of the solar cell, very high FF is obtainable. In this work, although the open-circuit voltage ($<580$ mV) is not high here, the efficiency of c-Si solar cell still reaches the state-of-the-art value (>20%) due to the high FF achieved.

Keywords: Si solar cell, Fill factor, Ag contact, MOS barrier

Background
Photoelectric conversion efficiency ($\eta$) of solar cell is determined by the product of open-circuit voltage ($V_{OC}$), short-circuit current density ($J_{SC}$), and fill factor (FF); therefore, achieving high $V_{OC}$ and $J_{SC}$ as well as FF is crucial for getting high $\eta$ [1, 2]. Considering the large abundance of Si on the earth's crust and the hyper amount of investment input in the Si solar cell industry, new approaches to enhance $V_{OC}$, $J_{SC}$, and/or FF for further increasing Si solar cell efficiency are always in demand. To our knowledge, FFs for the mostly efficient single crystalline- or c-Si solar cells reported so far are basically no larger than 0.835, for instance, for the PERL-type Si solar cell, FF = 0.828 ($V_{OC}$ = 706 mV, $J_{SC}$ = 42.7 mA/cm$^2$, $\eta$ = 25.0%) [3], for the IBC-type Si solar cell, FF = 0.830 ($V_{OC}$ = 730 mV, $J_{SC}$ = 41.2 mA/cm$^2$, $\eta$ = 25.0%) [4], for the HIT-type Si solar cell, FF = 0.835 ($V_{OC}$ = 738 mV, $J_{SC}$ = 40.8 mA/cm$^2$, $\eta$ = 25.1%) [5], and for the HIT + IBC type Si solar cell, FF = 0.827 ($V_{OC}$ = 740 mV, $J_{SC}$ = 41.8 mA/cm$^2$, $\eta$ = 25.6%) [6]. This work reports our finding of high FF (~0.87) and analyses of its origin based on an inverse connection of metal/oxide/semiconductor (Ag/SiO$_2$/Si) or MOS and PN junctions.

Methods
The substrate of the Si solar cell is P-type c-Si <100> wafer (two-sided polish, 10 x 10 x 0.2 mm$^3$ in size, 1–5 $\Omega$·cm). First, the Si wafer was degreased and ultrasonically cleaned and then dipped in diluted HF (1%). Then, it was placed in the boiling NaOH solution with concentration of 1 g/L at 90 °C for 30 min and rinsed in deionized water and blown dry to texture the surface for antireflection. A phosphorous paste was deposited on the front surface of Si, followed by annealing the wafer at temperature of 900 °C for 20 min in a tube furnace in nitrogen with purity of 99.999 % to form PN junction. A 60-nm-thick SiO$_2$ was evaporated by means of electron beam heating onto the top surface of now N$^+$ Si emitter for surface passivation [7] in a home-made vacuum chamber with a base pressure less than 1 × 10$^{-4}$ Pa. At the rear of the substrate, a 20-nm-thick Al$_2$O$_3$ was evaporated also by means of electron beam heating for rear passivation [7]. A 1.0-μm-thick Ag grid was then deposited onto the SiO$_2$ passivation layer as the front contact by resistance heating in another home-made vacuum chamber with a base pressure less than 1 × 10$^{-4}$ Pa.

© 2016 The Author(s). Open Access This article is distributed under the terms of the Creative Commons Attribution 4.0 International License (http://creativecommons.org/licenses/by/4.0/), which permits unrestricted use, distribution, and reproduction in any medium, provided you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons license, and indicate if changes were made.
the same system. Finally, the whole device was annealed in nitrogen atmosphere at 510 °C for 2 min followed by rapid thermal annealing (RTA) at 700 °C for 1 s. For RTA, we firstly pushed the sample from one end of the furnace tube to its middle within 3 s. The variation of temperature was from room temperature to 700 °C. Then, the sample was kept in the middle of the tube for 1 s, followed by being pulled out from the middle to the end of the tube within 3 s. All the processes of device fabrication were performed in a clean room. Its degree of cleanness was 100; that means, the number of dust particle with \( \phi \geq 0.5 \mu m \) was less than 3500/m³. The surface morphology was measured on a scanning electron microscope (SEM) (Philips, XL 30). The reflectance spectra were obtained with a spectrophotometer (Perkin-Elemer Lambda 900). The photovoltaic (PV) parameters of solar cells were measured on a solar simulator (Oriel/Newport, model 94023A) under 1-sun AM1.5G condition. In order to confirm the observed results of the high FF, the PV measurements were independently conducted on other two different solar simulators (Oriel/Newport, model 94043A, and Oriel/Newport, model 94023A). The external quantum efficiency (EQE) of the solar cell was acquired on a QE system of Oriel/Newport.

**Results and Discussion**

Figure 1 shows the schematic structure of c-Si solar cell prepared in this work as described above. Figure 2a gives the Si surface image after texturing. The pyramid-like nanostructures with average height of \( \sim 2 \mu m \) help to trap the incident light [8]. Figure 2b gives the measured EQE spectrum of the textured c-Si solar cell we prepared as shown in Fig. 1, which is termed cell A, and that of a plane c-Si solar cell. The surface reflectance spectra of Si before and after surface texturing are also plotted. It is seen that after surface texturing, the reflectance decreases significantly, and the lower reflectance yields higher EQE of the c-Si solar cell.

In Fig. 3a, a J-V (current density-voltage) curve of c-Si solar cell A is shown. Also shown are the J-V curves of the same solar cell before the final annealing, which is termed cell A−, and that was over-annealed (RTA at 700 °C for 30 s), which is termed cell A+. The PV parameters of the three cells are provided in Table 1. For cell A, \( V_{OC} = 572 \) mV, \( J_{SC} = 40.8 \) mA/cm², \( FF = 0.869 \), and \( \eta = 20.3 \) %. For cells A− and A+, the PV parameters all deteriorate severely, especially FF and \( \eta \). Note that the obtained FF (0.869) is considerably larger than the highest experimental one (≤0.835) reported [3–6].

In order to examine whether a charging effect of capacitance exists during the measurement, the J-V curve has been measured by scanning the voltage either from the lower voltage side to the higher one, or from the higher voltage side to the lower one, or to and fro repeatedly. They all remained the same. Hence, no charging effect exists.

Figure 3b gives the J-V curves of another solar cell prepared in a similar way as cell A, which is termed cell B. Its PV parameters are also listed in Table 1, which are quite close to those of cell A. Hence, the c-Si solar cell as shown in Fig. 3a is reproducible. Figure 3b also presents the J-V curves of the same cell B as measured.
We now investigate the origin of the very high FF. Firstly the $J$-$V$ curve of solar cell $A$ or $B$ is analyzed with the usual single PN junction solar cell model as described below [9],

$$J = J_{ph} - J_0 \cdot \left[ \exp \left( \frac{V_{PN} + J \cdot Rs}{n \cdot Vt} \right) - 1 \right] \cdot \frac{V_{PN} + J \cdot Rs}{R_p}$$  \hspace{2cm} (1)

where $V_{PN}$ is the voltage across the PN junction, $Vt = kT/e$, $T$ is absolute temperature, and $e$ is electron charge. $J_0$ means dark current density and $J_{ph}$ is photocurrent density. $R_s$ and $R_p$ are serial and parallel resistances, respectively. For the ideal situation when no recombination current exists in the depletion zone, $n$, the ideal factor, equals 1.0 and $R_s = 0$ and $R_p = \infty$. In reality, $n = 1$~2.

The experimental $J$-$V$ curve of cell $A$ in Fig. 3a is then fitted with Eq. (1). It is found that only when $n = 0.56$ can the calculated curve fit the experimental one well. However, the $n$ obtained here (0.56) is far less than 1.0, which is unphysical according to its definition. Recently, Richter et al. [10] have simulated the PV parameters of c-Si solar cell with the model of single PN junction. According to their simulations, it is unlikely to have the very high FF for the relatively low $V_{OC}$ as here (<600 mV). Therefore, the model of Eq. (1) is unable to explain the result of very high FF here.

We notice that the c-Si solar cell is actually composed of a PN junction and two metal/oxide/semiconductor or MOS junctions (Ag/SiO$_2$/N$^+$ Si and Al/Al$_2$O$_3$/P-Si). If the barrier heights of the two MOS junctions are very low, or if they are in Ohmic contacts with the PN junction, the $J$-$V$ curves of Si solar cell can still be described by Eq. (1) [11]. This is surely not the case according to the analysis above. In fact, the Ag/SiO$_2$/N-Si junction is inversely connected to the PN one; that is, the internally built-in fields of the two junctions are reverse in direction; while, Al/Al$_2$O$_3$/P-Si junction would be either forwardly connected to the PN one; that is, the built-in fields of the two junctions are the same in direction or be in Ohmic contact with the PN junction considering the P-type feature of the substrate [9~11].

The $J$-$V$ dependence of MOS junction cell can be described by Eq. (2) in the following [9, 11~17],

$$J = I_s \cdot \exp \left( \frac{V_{MOS}}{nS \cdot Vt} \right) \cdot \left[ 1 - \exp \left( -\frac{V_{MOS}}{Vt} \right) \right]$$  \hspace{2cm} (2)

where $I_s = A^* \cdot T^2 \cdot \exp(-\phi_B/Vt)$. $A^*$ means effective Richardson constant. $\phi_B$ is the barrier height. $nS$ is ideal factor of the MOS junction. For N-Si, $A^* = 112 \text{ A cm}^{-2} \text{ K}^{-2}$, and for P-Si, $A^* = 32 \text{ A cm}^{-2} \text{ K}^{-2}$ [17].

Figure 4 depicts the simulated $J$-$V$ curve of one PN junction solar cell, as calculated with Eq. (1) by using PV parameters of $V_{OC} = 572$ mV, $J_{SC} = 40.8$ mA/cm$^2$, $n = 1.06$, $R_s = 0.11 \Omega \cdot \text{cm}^2$, and $R_p = 8552 \Omega \cdot \text{cm}^2$. The PV parameters selected are taken from the fitting

---

**Table 1 PV parameters of the c-Si solar cells**

| Solar cell | $V_{OC}$ (mV) | $J_{SC}$ (mA/cm$^2$) | FF  | $\eta$ (%) |
|-----------|---------------|-----------------------|-----|------------|
| $A$ (700 °C, 1 s) | 572 | 40.8 | 0.869 | 20.3 |
| $A^-$ (no annealing) | 421 | 29.4 | 0.187 | 2.3 |
| $A^+$ (over-annealing) | 553 | 21.2 | 0.279 | 3.3 |
| $B$ | 576 | 40.4 | 0.868 | 20.2$^a$ |
| $B$ (SARI) | 579 | 40.1 | 0.867 | 20.1$^b$ |
| $B$ (SITP) | 578 | 40.6 | 0.867 | 20.3$^c$ |

$^a$Measured at Fudan University  
$^b$Measured at Shanghai Advanced Research Institute (SARI)  
$^c$Measured at Shanghai Institute of Technical Physics (SITP)
results as will be explained in the following. The $J$-$V$ curve of the MOS junction solar cell was calculated with Eq. (2) by using the same $J_{SC}$ (40.8 mA/cm$^2$), with $ns = 1.21$, and $\phi_B = 0.505$ eV, which are also from the following fitting results. For the case of forward connection, or the model of PN + MOS,

$$V = V_{PN} + V_{MOS}$$

(3)

and for the case of inverse connection, or the model of PN-MOS,

$$V = V_{PN} - V_{MOS}$$

(4)

To simulate the $J$-$V$ curve of PN + MOS or PN-MOS, a numerical calculation procedure was used; that is, starting from $J = J_{SC}$ down to $J = 0$, for each point of $J$ (the step of $J$ was chosen 0.1 mA/cm$^2$), both $V_{PN}$ and $V_{MOS}$ were calculated by Eqs. (1) and (2), respectively, combining all the other selected PV parameters. Then, Eqs. (3) and (4) were applied to get the total voltage across the solar cell for the models of forward and inverse connections, respectively. The resulting $J$-$V$ curves of PN + MOS and PN-MOS are given in Fig. 4, too. It is clear that for the forward connection, FF even becomes lower; while, for the inverse connection, higher FF is available. It should be pointed out that it is only when $\phi_B/e$ of the MOS junction is not far from $V_{OC}$ of the solar cell, which is the case during the simulation of Fig. 4, could a high FF be obtained. In fact, we have simulated the relation between FF and $\phi_B$. It is found that when $\phi_B/e$ is very close to or even equals $V_{OC}$, FF larger than 0.9 can be obtained.

We then use the model of PN-MOS to fit the $J$-$V$ curve of cell A with Eqs. (1) and (2). The fitting curve has been plotted in Fig. 3a. At this moment, the derived PV parameters are $n = 1.06$, $ns = 1.21$, $\phi_B = 0.505$ eV, $Rs = 0.11$ Ω·cm$^2$, and $Rp = 8552$ Ω·cm$^2$. The values of $n$ and $ns$ are now rational, and $\phi_B/e$ is close to $V_{OC}$ (although not very close to 0.572 V), which is consistent with the inference derived above.

It needs to be pointed out that all the PV parameters including FF are very sensitive to the annealing conditions, as have been illustrated in Fig. 3a. If there is no annealing or the annealing is insufficient, the barrier height and the serial resistance would become larger [18–20], which could severely degrade the performance of solar cell. On the other hand, if the annealing is over-done, Ag will easily penetrate through SiO$_2$ and into the emitter zone or even into the PN junction, then the whole device would be ruined. The RTA is mainly used to modulate the barrier height of MOS junction, so a proper RTA is crucial to get a very high FF. On the other hand, the thickness of SiO$_2$ also influences FF as well as $V_{OC}$ and $J_{SC}$, via influencing Ag diffusion and barrier height of the MOS junction. An optimized combination of annealing and SiO$_2$ thickness has been performed here to achieve a high efficiency.

Conclusions

In summary, we have obtained high FFs (~0.87) of c-Si solar cells by using Ag contact as front electrode after proper annealing and rapid thermal annealing treatments. Our model analysis indicates that the very high FF is caused by the inverse connection of MOS (Ag/SiO$_2$/Si) and the PN junctions, with the MOS junction possessing a barrier height/e close to $V_{OC}$. By using this approach, c-Si solar cells with efficiencies >20 % are achieved due to their high FFs, although their open-circuit voltages are not high (<580 mV) here. It is expected that further improvements on increasing open-circuit voltage and meanwhile remaining the very high FF could lead to further higher efficiency.

Abbreviations

- $e$: Electron charge; EQE: External quantum efficiency; FFs: Fill factors; $J_0$: Dark current density; $J_{ph}$: Photocurrent density; $J_{SC}$: Short-circuit current density; MOS: Metal/oxide/semiconductor; $n$: The ideal factor of the PN junction; $ns$: Ideal factor of the MOS junction; PV: Photovoltaic; $R_p$: Parallel resistance; Rs: Serial resistances; RTA: Rapid thermal annealing; SARI: Shanghai Advanced Research Institute; SEM: Scanning electron microscope; SITP: Shanghai Institute of Technical Physics; $T$: Absolute temperature; $V_{OC}$: Open-circuit voltage; $\eta$: Conversion efficiency; $\phi_B$: The barrier height

Acknowledgements

This work is supported by the National Basic Research Program of China (973 Program), Grant No. 2012CB934303, and the National Natural Science Foundation of China under Grant Nos. 61275178 and S1472051.

Authors’ Contributions

LXW prepared all the samples and measured the SEM and I-V data. ZQZ measured the QE data and I-V data. TNZ and XC measured the reflectance data and I-V data. ML designed the experiments and wrote the manuscript. All authors read and approved the final manuscript.

Competing Interests

The authors declare that they have no competing interests.
Author details
1Department of Optical Science and Engineering, and Shanghai Ultra-Precision Optical Manufacturing Engineering Center, Fudan University, Shanghai 200433, China. 2Thin Film Optoelectronic Technology Center, Shanghai Advanced Research Institute, Chinese Academy of Sciences, Shanghai 201210, China. 3Shanghai Institute of Technical Physics, Chinese Academy of Sciences, Shanghai 200083, China.

Received: 19 July 2016 Accepted: 5 October 2016

Published online: 10 October 2016

References
1. Green MA (1981) Solar cell fill factors: general graph and empirical expressions. Solid State Electron 24:788–789
2. Romero B, Pozo GD, Arredondo B (2012) Exact analytical solution of a two diode circuit model for organic solar cells showing s-shape using lambert w-functions. Sol Energy 86:3026–3029
3. Zhao J, Wang A, Green MA, Ferrazza F (1998) 19.8% efficient “honeycomb” textured multicrystalline and 24.4% monocrystalline silicon solar cells. Appl Phys Lett 73:1991–1993
4. Smith DD, Cousins P, Westerberg S, Jesus-Tabajonda RD, Aniero G, Shen Y (2014) Toward the practical limits of silicon solar cells. IEEE J Photovolt 4:1465–1469
5. Adachi D, Hernández JA, Yamamoto K (2015) Impact of carrier recombination on fill factor for large area heterojunction crystalline silicon solar cell with 25.1% efficiency. Appl Phys Lett 107:73–812
6. Masuko K, Shigematsu M, Hashiguchi T, Fujishima D, Kai M, Yoshimura N, Yamanishi T (2014) Achievement of more than 25% conversion efficiency with crystalline silicon heterojunction solar cell. IEEE J Photovolt 4:1433–1435
7. Qi T, Wang L, Hao H, Shi W, Lu M (2015) A synergistic effect of surface texture and field-effect passivations on improving silicon solar cell performance. Physica E Low-dimensional Systems and Nanostructures. 71:96-100.
8. Zhou J, Facsko S, Lu M, Müller W (2011) Nanopatterning of silicon surfaces by normal incident ion erosion: influence of iron incorporation on surface morphology evolution. J Appl Phys 109:645–647
9. Sistema SM (1981) Physics of semiconductor devices. Wiley, New York, pp.245-311
10. Richter A, Hermle M, Glunz SW (2013) Reassessment of the limiting efficiency for crystalline silicon solar cells. IEEE J Photovolt 3:1184–1193
11. Rhoderick EH, Williams RH (1988) Metal–semiconductor contacts. Clarendon, Oxford, pp.89–116
12. İkram ORAK, Turut A, Toprak M (2015) The comparison of electrical characterizations and photovoltaic performance of Au/p-Si and Al/azure c/p-Si junctions devices. Synthetic Met 206:65–73
13. Siad M, Keffous A, Mamma S, Belkacem Y, Menari H (2004) Correlation between series resistance and parameters of Al/N-Si and Al/p-Si Schottky barrier diodes. Appl Surf Sci 236:366–376
14. Okutan M, Yakuphanoglu F (2008) Analysis of interface states and series resistance of Ag/SiO2/Al-silicon diode using current–voltage and impedance spectroscopy methods. Microelectron Eng 85:646–653
15. Keffous A, Siad M, Cheriet A, Benrekaa N, Belkacem Y, Menari H, Cherqui W, Dahmani A (2004) Comparison of electrical and optical parameters of Au/N-Si and Ag/N-Si Schottky barrier photodiodes. Appl Surf Sci 236:42–49
16. Altuntas H, Bingi A, Aydemir U, Asar T, Cetin SS, Kars I, Alhindal S, Ozcelik S (2009) Electrical characterization of current conduction in Au/TiO2/N-Si at wide temperature range. Mat Sci Semicon Proc 12:224–232
17. Andrews JM, Lepselter MP (1968) Reverse current-voltage characteristics of metal-silicide Schottky diodes. Solid State Electron 13:1011–1023
18. Qi B, Wang J (2013) Fill factor in organic solar cells. Phys Chem Chem Phys 15:8972–8982
19. Feldmann F, Simon M, Bivour M, Reichel C, Hermle M, Glunz SW (2014) Efficient carrier-selective p- and n-contacts for Si solar cells. Sol Ener Mat Sol C 131:100–104
20. Banu PK, Law F, Vindoth S, Kumar A, Richter P, Bottari F, Hoex B (2014) 0.4% absolute efficiency increase for line-edge-diffused screen-printed multicrystalline silicon wafer solar cells by non-acidic deep emitter etch-back. Sol Ener Mat Sol C 137:193–201