Trapping of single nano-objects in dynamic temperature fields
Marco Braun, Frank Cichos, Alois Würger

To cite this version:
Marco Braun, Frank Cichos, Alois Würger. Trapping of single nano-objects in dynamic temperature fields. Physical Chemistry Chemical Physics, Royal Society of Chemistry, 2014, 16, pp.15207. 10.1039/c4cp01560f. hal-01025336

HAL Id: hal-01025336
https://hal.archives-ouvertes.fr/hal-01025336
Submitted on 18 Jul 2014

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Trapping of Single Nano-objects in Dynamic Temperature Fields

Marco Braun and Frank Cichos*
Molecular Nanophotonics Group, Institute of Experimental Physics I, University of Leipzig, 04103 Leipzig, Germany

Alois Würger
LOMA, Université de Bordeaux CNRS, 351 cours de la Libération, 33405 Talence, France

In this article we explore the dynamics of a Brownian particle in a feedback-free dynamic thermophoretic trap. The trap contains a focused laser beam heating a circular gold structure locally and creating a repulsive thermal potential for a Brownian particle. In order to confine a particle the heating beam is steered along the circumference of the gold structure leading to a non-trivial motion of the particle. We theoretically find a stability condition by switching to a rotating frame, where the laser beam is at rest. Particle trajectories and stable points are calculated as a function of the laser rotations frequency and are experimentally confirmed. Additionally, the effect of Brownian motion is considered. The present study complements the dynamic thermophoretic trapping with a theoretical basis and will enhance the applicability in micro- and nanofluidic devices.

PACS numbers:

I. INTRODUCTION

Single particle trapping is of high importance for long-time studies of single molecules or particles in solution without mechanical immobilization. This demand led to the development of traps to counter-act Brownian motion following different approaches. Optical forces can efficiently manipulate objects with sufficiently large dielectric contrast to the solvent. Quadrupole traps such as the Paul trap have been developed over half a century to trap ions in vacuum by high-frequency electric quadrupole fields and are applied in various fields such as mass spectroscopy and quantum information processing. In viscous media quadrupole traps are realized by utilizing dielectrophoresis and electrophoresis. Recently, Paul trapping of single submicron-sized particles in aqueous solution has been demonstrated [1]. Single molecule trapping efficiency is achieved with ABEL trapping which relies on adaptively controlled electric fields. Independently from the electronic properties, particles can be trapped e.g. by hydrodynamic flow [2] or acoustic waves [3].

Temperature gradients have also been demonstrated for particle and macromolecular manipulation [4, 5], since they interact on both non-ionic and charged solutes through thermophoresis, an umbrella term for thermally induced motion at a velocity which is proportional to the temperature gradient [6, 7]. One prominent effect which leads a charged particle going from the hot to the cold is caused by the temperature induced perturbation of its electric double-layer without applying a strong electric field. Recently, a method was proposed to trap single particles in a quasi-static temperature landscape that is produced by a photothermally heated gold structure [8]. In the simplest case, such a structure consists of a circular hole in a gold film of several microns in diameter. By illuminating this gold structure by means of an expanded laser beam, a steady-state temperature field is generated capable of trapping a single particle within a local temperature minimum in a film of solvent above the center of the circular hole.

In the present paper stronger temperature gradients are achieved by heating the edge of the Au hole using a focused laser beam, as sketched in Fig. 1a. Also, for such a heating scheme, the object of interest in the center of the trap is not under direct illumination by the heating beam, preventing e.g. bleaching. However, for a typically positive thermodiffusive coefficient leading a particle to move to a colder region, a steady-state heating by means of a focused laser beam will end up in a purely repulsive thermal potential forcing a particle out of the trap immediately. Hence, to prevent the particle from escaping the trap, the laser beam needs to be steered. Inspired by the Paul trap, here, we drive the laser beam along the circumference of a hole in a gold film at a frequency $f = \omega/2\pi$ leading the thermal potential to rotate (Fig. 1a). Due to a net inward component of the thermophoretic drift a confinement for a particle can be achieved in the center of the trap.

In the following we demonstrate the feasibility of a thermophoretic particle trap using time-dependent temperature gradients. We give a detailed study of the dynamic properties of a particle. We theoretically investigate the trapping stability and determine the stationary trajectories as a function of the thermophoretic drift velocity and the rotation frequency which are experimentally confirmed. In a second step, we account for Brownian motion and determine the probability density in the thermal trapping potential.

Thermalization of the plasmonic excitation occurs at a time-scale of microseconds. Hence, the temperature field follows almost instantaneously the rotation laser. Because of the different heat conductivity of gold and water, the resulting temperature profile is not isotropic but significantly smeared out along the edge of the gold film, as shown by the numerical simulation results of Fig. 1, b–d). This distortion, however, is of minor importance for our purpose, since thermophoretic trapping relies mainly on
FIG. 1: a) Sketch of the sample: A circular gold structure is heated by a focused laser beam. b) Simulated temperature field produced by the optically heated gold film. The dashed green circle indicates the edge of the gold structure. c) Temperature profile along the gold edge in the plane of the gold structure (black) and 300 nm above (dashed red). d) temperature line profile in the plane of the gold structure (black) and 300 nm above (dashed red). The green line indicated the laser profile (in a.u.).

The experimental results of the particle dynamics in a rotating temperature field reveal some general features, which we want to highlight before starting with an in depth description of the particle motion.

II. PARTICLE DYNAMICS IN THE ROTATING FRAME

The experimental results of the particle dynamics in a rotating temperature field reveal some general features, which we want to highlight before starting with an in depth description of the particle motion. Fig. 2a) and b) display the positional distribution of a single 460 nm PS bead in the same trap structure with equal heating laser intensity but at different laser rotation frequencies of 100 Hz and 0.7 Hz. Both trajectory point distributions indicate the confinement of the particle in the rotating temperature field. However, while the magnitude of the thermal drift is only dependent on the heating laser intensity and does not change with rotation frequency, the inward component of the thermal drift seems to decrease for a slower rotation frequency. Due to the rotating laser field, a tangential component of the particle drift should appear as well. The particle dynamics should therefore depend on this tangential drift at slow frequency too. This importance of tangential and radial drift in the trap structure is better recognized when transforming the coordinate system in to the frame moving with the laser beam. In such a frame the laser beam and the temperature profile are at rest but the sample including the fluid rotates counter-clockwise around the center of the trap. Fig. 2c) shows the data at 0.7 Hz transformed to the rotating frame. The position of the heating beam is indicated by the green dot. The particles position distribution is Gaussian but asymmetric and the maximum shifted from the center of the trap. These features are readily understood in terms of the thermophoretic repulsion from the laser position and the advection by the rotating flow, and imply in particular that the particle is always in front of the laser spot. Transforming back to the lab frame smears out the asymmetry, and one recovers the broadened position distribution of Fig. 2b). The arrows in Fig. 2c) indicate the particle velocity with respect to the rotating frame. They reveal a circular motion around the center of the distribution function. These effects will be studied in detail.

III. STATIONARY POINTS IN THE FLOW FIELD

The particle dynamics originates from the thermal forces, advection, and Brownian motion. As a first step, we discard Brownian motion and retain the deterministic part only. Due to the aqueous solvent and small particle size the Reynolds number is low $Re \sim 10^{-6}$, i.e. viscous forces dominate the motion of the particle. In this overdamped limit, inertia may be neglected and the particle instantaneously follows the thermal and advection drift. Then the particle velocity field in the rotation frame can be written as the sum

$$\mathbf{u} = \mathbf{v}_T + \mathbf{\omega} \times \mathbf{r}$$

(1)
of the thermophoretic drift velocity $\mathbf{v}_T = -D_T \nabla T(r)$ with the thermodiffusion coefficient $D_T$ at the position $r$ with respect to the center of the trap and the advection by the rotating fluid with $\omega = \omega e_z$. In the following we assume an isotropic temperature profile as mentioned above, which implies that the gradient decays as $\nabla T = -Q/(4\pi R^3)$, with $R = |r - a\Theta_0|$ being the distance from the laser position.

In Fig. 3a we plot the calculated flow field $\mathbf{u}(x, y)$ in the upper-right quadrant of the trap for a given set of parameters. The flow field shows two fix points, where the thermophoretic drift $\mathbf{v}_T$ and the advection drift $\omega \times r$ cancel each other such that the particle flow vanishes $\mathbf{u} = 0$ (see Fig. 3b). The upper one is unstable. A slight perturbation is amplified and the particle either escapes to infinity or moves towards the lower fix point, which is stable. The flow field around this fix point appears to be spiraling towards this fix point. As the flow field is depicted in the rotating frame, a particle in this fix point would carry out a circular motion around the trap center in the lab frame when neglecting Brownian motion.

We further determine the position of the fix points in the trap as a function of laser rotation frequency $\omega$ and the thermophoretic velocity $v_T$. Inserting the temperature gradient into equation 1 and setting $\mathbf{u} = 0$ yields two real solutions, which correspond to the positions of the above described fix points. Both solutions lie on a half circle described by $x^2 = y(a - y)$ as indicated by the green line in Fig. 3b. The coordinates of the fix points may be expressed in terms of the dimensionless parameter

$$\xi = \frac{\omega a}{u_T}$$

which is given by the ratio of the tangential laser velocity $\omega a$ and the thermophoretic velocity $u_T$.

$$u_T = D_T \frac{Q}{4\pi \kappa a^2}.$$  

The cartesian coordinates of the stable fix point are then given by a power series in $\xi$ by $y_0 = a(\xi^2 + 2\xi^{-4} + ...) \quad \text{and} \quad x_0 = \sqrt{y_0(a - y_0)}$.

Similarly the position of the stable fix point may also be expressed in polar coordinates given by the distance $r_0$ from the trap center

$$r_0 = \frac{1}{\xi} + \frac{1}{\xi^3} + ...$$

and the angle $\varphi_0$ when $\tan \varphi_0 = \frac{1}{\xi} + \frac{3}{2\xi^3} + ...$. The exact coordinates of the fix points are reported in the supplement.

The above equations immediately reveal that both stationary points exist only for a sufficiently large value of $\xi > \xi_{\text{min}} = \sqrt{27/4} \approx 2.598$. This means that the tangential velocity of the laser on the circumference of the trap has to be larger than the thermophoretic velocity by a factor of 2.598. If this stability condition is not fulfilled, the rotating laser is to slow to prevent the particle from being pushed out of the trap by the thermal drift. In the case $\xi = \xi_{\text{min}}$, both fix points are located at the same position on the half circle. When increasing $\xi$ further they repel each other and the stable fix point is approaching the center of the trap. With typical experimental parameters, $u_T \sim \mu$m/s and $a \sim \mu$m, one finds a minimum frequency of $\omega/2\pi \sim 1$Hz.

These theoretical findings agree well with experimental data obtained for a single 460 nm PS bead in water recorded at different laser rotation frequencies $\omega$. At
each frequency, the particle positions have been recorded and were transformed to the rotating frame. Figure 4a displays the corresponding histograms of the particle positions for three different laser rotation frequencies and already reveals the shift of the fix point towards the trap center with increasing rotation frequency $\omega$. The distance of the histogram maximum for different laser rotation frequencies follows nicely the predicted frequency dependence. Fitting the radial distance as a function of frequency (eq. 3) in Fig. 4b directly yields a thermophoretic velocity of $u_T = 3.3 \mu m/s$ at the trap radius of $a = 4.3 \mu m$. The $x, y$ positions of the measured maxima are consistently below the half circle $x^2 = y(a - y)$ (Figure 4c, grey squares). While the radial distance $r_0$ is matched by the theory, the phase $\varphi_0$ is preceding the theoretical phase due to the fact that the real heat source is smeared out along the rim of the gold structure (see Fig. 1a), while we model the behavior with a point heat source. We estimate a resulting shift in angle to be $\Delta \varphi_0 \approx 10^\circ$. The corrected data is shown with the colored squared Fig. 4c and follows the half circle indicated by the green line.

IV. MOTION CLOSE TO THE STATIONARY POINT

While the flow field already indicates the two different fix points we can analyze the motion of the particle close to the tentatively stable fix point in more detail. We therefore linearize the flow $\mathbf{u}(\mathbf{r})$ at the distance from the stationary point, $\mathbf{r} = \mathbf{r} - \mathbf{r}_0$, and then expand in powers of $1/\xi$

$$\mathbf{u} = \omega \times \mathbf{r} + \frac{\omega}{\xi} (\mathbf{e}_x \hat{x} - 2 \mathbf{e}_y \hat{y}) + ...$$

(4)

where we have discarded terms of $O(\xi^{-2})$. The first term describes the rotation around the stationary point with frequency $\omega$.

The second term, which is by a factor $\xi$ smaller and therefore independent of $\omega$, accounts for the radial flow with respect to the fix point at $\mathbf{r}_0$. The flow along the $\hat{x}$-direction with velocity $\omega \hat{x}/\xi = u_T \hat{x}/a$ is oriented outward, whereas along the $\hat{y}$-direction there is an inward flow toward the fixed point with twice the velocity $-2 \omega \hat{y}/\xi = -2 u_T \hat{y}/a$. When averaging over one cycle one finds that there is a net inward flow towards the stationary point $\mathbf{r}_0$, which proofs the stable nature of this fix point.

Eq. (4) can be integrated to the following form,

$$\begin{align*}
\hat{x}(t) &= A e^{-T \Gamma} \cos(\Omega t - \phi), \\
\hat{y}(t) &= A e^{-T \Gamma} \sin(\Omega t),
\end{align*}$$

(5)

a spiral trajectory, where $A$ is the initial amplitude, $\Omega = \omega \sqrt{1 - \frac{x^2}{a^2}}$ the frequency, $\Gamma = u_T/(2a)$ a damping coefficient and $\phi = \frac{\xi}{2} - 1$ the phase describing the asymmetry. Without taking thermal fluctuations into account the particle will converge to the fix point on a spiral in the rotating frame for $t \rightarrow \infty$ if the stability condition $\xi > \xi_{\text{min}}$ is fulfilled. Once the fix point is reached, the particle travels in circles around the center of the trap in the lab frame. $\Gamma$ can be interpreted as a relaxation rate describing how fast a particles reaches the stable point, which is independent of $\omega$. Hence, while increasing $u_T$ and $\omega$ by the same factor does not influence the position of the stable point, it amplifies the net inward flow.

![Figure 4](image-url)

**FIG. 4:** a) Position distribution histograms in the rotating frame for 0.6 Hz (top), 1.1 Hz (center) and 2.7 Hz (bottom). b) Distance of the central point of the positional distribution as a function of the rotation frequency with fit of equation 3. c) Position of the central point of the positional distributions, i.e. the positions of the stable point for different rotation frequencies. All points are tilted by 10° around the origin to compensate for the finite extend of the heat source in the experiment. The green arc again indicates the line $x^2 = y(a - y)$. The frequency is color-coded and can be read from the plot in c. The grey squares is the uncorrected data.
The phase $\phi$ determines the skewness of the trajectory, which reduces to a circle for $\phi = 0$, for high laser rotation frequencies.

A vector plot of an experimentally observed velocity field $u(x, y) = (u_x(x, y), u_y(x, y))$ in the rotating frame is shown in Figure 5 for the lowest measured frequency of $f = 0.6$ Hz ($\xi = 4.9$). Each arrow represents the average direction of the particle in the according region, such that the stochastic Brownian motion of the particle averages out. To compare the data to the theoretical description, we plotted the velocities separated in $x$ and $y$-direction along the horizontal (green) and vertical (magenta) lines in figures 5b and 5c. Correspondingly, the black lines were calculated from equations 5 with $f = \omega/2\pi = 0.6$ Hz, $a = 4.3 \mu$m and $u_T = 3.3 \mu$m/s which was found from the fit of eqn. 3 in Fig. 4c. As can be seen, the theory and experimental data agree very well.

Although working at much lower frequencies, the motion that is observed for a particle in a thermal trap with a rotating temperature field exhibits strong similarities to the motion of ions in a Paul trap, which travel on non-trivial trajectories within the trap. Depending on the stability parameters a macro-motion is observed superimposed with the micro-motion at the frequency of the rotating quadrupole field. In our description of the thermal trap we decoupled the micro-motion at $\omega$ by switching to the rotating frame. Within this frame, we observe a harmonic oscillation (macro-motion) at a frequency $\Omega$ which also depends on the trapping parameters. However, due to the viscous damping at low Reynolds number in the thermal trap this macro-motion disappears exponentially and the particle reaches the stable point in the long time limit whereas it sustains for ion trapped in vacuum.

Eqs. (5) resemble a solution of a two-dimensional damped harmonic oscillator. Hence, from this trajectory it is clear that the particle is confined in an effective anisotropic harmonic potential in the rotating frame, leading to an anisotropic Gaussian positional distribution.

V. PROBABILITY DISTRIBUTION

So far we have not taken into account the Brownian motion of the particle. The corresponding convection-diffusion problem is described by the stationary Smoluchowski equation for the particle concentration,

$$\nabla \cdot \mathbf{J} = 0, \quad \mathbf{J} = c \mathbf{u} - D \nabla c.$$  \hspace{1cm} (6)

Because of the rather intricate velocity field $\mathbf{u}$ there is no general analytical solution. In the following we derive an approximate steady-state distribution function.

The drift velocity (4) is linearized in powers of $\hat{x}$ and $\hat{y}$. Its radial and angular components read to leading order in $1/\xi$, \begin{align} u_r &= \frac{\omega \hat{x}^2 - 2 \hat{y}^2}{\hat{r}}, \quad u_\phi = \omega \hat{r}. \end{align} \hspace{1cm} (7)

FIG. 5: a) Experimental flow field calculated from the trajectory for a rotation frequency of $f = 0.6$ Hz. The green dot indicated the position of the heated spot. The red dot shows the location of the stationary point. Note that in this image the length of the arrow does not represent $|\mathbf{u}|$. b) and c) Flow velocities in $x$ and $y$-direction along the green and magenta lines in a). The black lines are not fits, but calculated according to eqns 5 for a trap radius $a = 4.3 \mu$m and $u_T = 3.3 \mu$m/s as obtained earlier.
Note that the radial drift occurs outward along the \( \hat{x} \)-axis and towards the center along the \( \hat{y} \)-axis. Thus without the angular motion, the particle would escape within the cones \( \hat{x}^2 - 2\hat{y}^2 > 0 \). Yet since both radial drift and diffusion are slow as compared to the angular motion, the distance \( \hat{r} \) changes rather little during one cycle.

Thus we may, in a first approximation, replace the radial velocity with its time average \( \bar{u}_r \). From (5) one finds \( \bar{u}_r = -u_T \frac{\hat{\phi}}{2a} \).

Since \( u_T > 0 \), there is an effective drift towards the stationary point. Thus trapping arises from the superposition of the fast angular motion and the minus sign of the mean radial velocity \( \bar{u}_r \). The stationary state is obtained requiring that the radial current \( J_r = \bar{u}_r = Dd\bar{c}/d\hat{r} \) vanishes. Solving \( J_r = 0 \) results in the Gaussian probability distribution \( c = c_0 e^{-\hat{r}^2/2\sigma^2} \), where the mean-square distance

\[
\sigma^2 = \frac{2Da}{u_T}
\]

is determined by the ratio of the diffusion coefficient and the thermophoretic velocity.

Both from the stream lines in Fig. 3 and from the trajectories (5), it is clear, however, that \( c(\hat{x}, \hat{y}) \) is not isotropic in the \( \hat{x} - \hat{y} \)-plane. The anisotropy is best expressed in terms of the non-zero correlation \( \hat{x}\hat{y} = \frac{1}{2}\hat{r}^2 \sin \phi \), which follows directly from (5). The correlation matrix is diagonalized by adopting skew coordinates \( \hat{r}_\pm = (\hat{x} \pm \hat{y})/\sqrt{2} \), resulting in the steady-state distribution

\[
c(\hat{x}, \hat{y}) = c_0 \exp \left( -\frac{\hat{r}_+^2}{2\sigma_+^2} - \frac{\hat{r}_-^2}{2\sigma_-^2} \right),
\]

with mean-square displacements

\[
\sigma_\pm^2 = (1 \pm \sin \phi) \frac{2Da}{u_T}.
\]

By expanding in inverse powers of \( \xi \), we find \( \sin \phi = \frac{3}{2\xi} \). This parameter is largest at small frequency and decreases with increasing \( \omega \). At large frequency the widths \( \sigma_\pm \) become equal, the trajectory in the trap approaches a circle, and the probability distribution reduces to (9).

Equations 10 and 11 can be directly compared to the experimental data (Figure 6). Although the data points of \( \sigma_+ \) and \( \sigma_- \) do not quantitatively follow the predictions in Figure 6a, it can clearly be seen that the average values of the width are consistent with the theory. Also, the anisotropy \( \sigma_+ / \sigma_- \) is clearly visible for low rotation frequencies and disappears for higher frequencies as expected.

The parameters \( \sigma_\pm \) give the width of the trapping potential in the rotating frame. They are determined by the ratio of advective and diffusive transport rates and hence are inversely proportional to the square-root of the Péclet number \( Pe = u_T a / D \). In the experiment, with a diffusion coefficient of \( D = 0.59 \mu m^2 / s \), a thermal drift of \( u_T = 3.3 \mu m / s \) and a trap radius of \( a = 4.3 \mu m \) a Péclet number of \( Pe \approx 24 \) is achieved. The widths are also inversely proportional to the the square-root of the Soret coefficient and excess temperature \( \sigma_\pm \propto (S_T \Delta T)^{1/2} \) similar as found in [8].

VI. CONCLUSION

We have studied the motion of a single colloidal particle in a dynamic feedback-free thermal trap using a rotating temperature field to create confinement. Since the temperature field is repulsive for the colloidal particles, the confinement is the result of the dynamics of the temperature field and requires a certain threshold rotation
frequency. For frequencies below this threshold particles are pushed out of the trap, while above the threshold a metastable and a stable trapping point exist. The motion of the particles around the stable fix point is reminiscent of the complex motion in an electrodynamic Paul trap. The particle motion, however, is strongly damped as compared to the ion motion in the Paul trap due to the viscous environment. The theoretical findings are well supported by experiments confirming the main characteristics of the motion and provide a first glimpse on how single particle or even single molecule motion might be manipulated with dynamic temperature fields.

VII. MATERIALS AND METHODS

The preparation of the gold structure is fully analogous to a previous publication [8]. A clean glass substrate is coated by 5 nm chromium film, an adhesion layer for the gold structure. Isolated polystyrene beads (∼ 8 µm diameter) are prepared on a glass substrate by spin coating. After coating the glass with the beads with a 50 nm gold layer by thermal evaporation, the beads are removed by sonication and toluene. The gold film with circular holes of about 8 µm diameter remains on the glass substrate. The chromium film uncovered by the gold is removed by etching. The experimental sample consists of two parallel glass slides, where the lower one carries the gold structure. A water film of about 700 nm thickness is confined between the glass slides. The water film contains dye-doped colloidal PS beads of 460 nm diameter. The motion of the colloidal particles is monitored by wide-field fluorescence microscopy, where the fluorescence is excited at 532 nm wavelength by an expanded laser beam (ω₀, w ≈ 20 µm), collected by an Olympus lens (100x/1.4) and imaged onto an Andor Ixon EMCCD camera. A framerate of 100 Hz was used at a 2 × 2 binning. An additional focused laser beam (ω₀, h ≈ 20 µm) also of 532 nm wavelength can be steered in the sample plane with the help of an acousto-optic deflector (AOD) and is used for the plasmonic heating of the gold structure. The heating laser spot is driven in circles along the circumference of the gold structure at a rotation frequency f = ω/2π.

[1] W. Guan, S. Joseph, J. H. Park, P. S. Krstic, and M. A. Reed, Proceedings of the National Academy of Sciences (2011).
[2] M. Tanyeri and C. M. Schroeder, Nano Letters 13, 2357 (2013), http://pubs.acs.org/doi/pdf/10.1021/nl4008437, URL http://pubs.acs.org/doi/abs/10.1021/nl4008437.
[3] B. Qian, D. Montiel, A. Bregulla, F. Cichos, and H. Yang, Chem. Sci. 4, 1420 (2013), URL http://dx.doi.org/10.1039/C2SC21263C.
[4] H.-R. Jiang, N. Yoshinaga, and M. Sano, Phys. Rev. Lett. 105, 268302 (2010), URL http://link.aps.org/doi/10.1103/PhysRevLett.105.268302.
[5] Y. T. Maeda, A. Buguin, and A. Libchaber, Phys. Rev. Lett. 107, 038301 (2011), URL http://link.aps.org/doi/10.1103/PhysRevLett.107.038301.
[6] R. Piazza and A. Parola, Journal of Physics: Condensed Matter 20, 153102 (2008), URL http://stacks.iop.org/0953-8984/20/i=15/a=153102.
[7] A. Würger, Reports on Progress in Physics 73, 126601 (2010), URL http://stacks.iop.org/0034-4885/73/i=12/a=126601.
[8] M. Braun and F. Cichos, ACS Nano 0, null (0), http://pubs.acs.org/doi/pdf/10.1021/nn404980k, URL http://pubs.acs.org/doi/abs/10.1021/nn404980k.