Abstract

We present a model of unsupervised phonological lexicon discovery—the problem of simultaneously learning phoneme-like and word-like units from acoustic input. Our model builds on earlier models of unsupervised phone-like unit discovery from acoustic data (Lee and Glass, 2012), and unsupervised symbolic lexicon discovery using the Adaptor Grammar framework (Johnson et al., 2006), integrating these earlier approaches using a probabilistic model of phonological variation. We show that the model is competitive with state-of-the-art spoken term discovery systems, and present analyses exploring the model’s behavior and the kinds of linguistic structures it learns.

1 Introduction

One of the most basic problems of language acquisition is accounting for how children learn the inventory of word forms from speech—phonological lexicon discovery. In learning a language, children face a number of challenging, mutually interdependent inference problems. Words are represented in terms of phonemes, the basic phonological units of a language. However, phoneme inventories vary from language to language, and the underlying phonemes which make up individual words often have variable acoustic realizations due to systematic phonetic and phonological variation, dialect differences, speech style, environmental noise, and other factors. To learn the phonological form of words in their language children must determine the phoneme inventory of their language, identify which parts of the acoustic signal correspond to which phonemes—while discounting surface variation in the realization of individual units—and infer which sequences of phonemes correspond to which words (amongst other challenges).

Understanding the solution to this complex joint-learning problem is not only of fundamental scientific interest, but also has important applications in Spoken Language Processing (SLP). Even setting aside additional grammatical and semantic information available to child learners, there is still a sharp contrast between the type of phonological learning done by humans and current SLP methods. Tasks that involve recognizing words from acoustic input—such as automatic speech recognition and spoken term discovery—only tackle parts of the overall problem, and typically rely on linguistic resources such as phoneme inventories, pronunciation dictionaries, and annotated speech data. Such resources are unavailable for many languages, and expensive to create. Thus, a model that can jointly learn the sound patterns and the lexicon of a language would open up the possibility of automatically developing SLP capabilities for any language.

In this paper, we present a first step towards an unsupervised model of phonological lexicon discovery that is able to jointly learn, from unannotated speech, an underlying phoneme-like inventory, the pattern of surface realizations of those units, and a set of lexical units for a language. Our model builds on earlier work addressing the unsupervised discovery of phone-like units from acoustic data—in particular the Dirichlet Process Hidden Markov Model (DPHMM) of Lee and Glass (2012)—and the un-
supervised learning of lexicons from unsegmented symbolic sequences using the Adaptor Grammar (AG) framework (Johnson et al., 2006; Johnson and Goldwater, 2009a). We integrate these models with a component modeling variability in the surface realization of phoneme-like units within lexical units.

In the next section, we give an overview of related work. Following this, we present our model and inference algorithms. We then turn to preliminary evaluations of the model’s performance, showing that the model is competitive with state-of-the-art single-speaker spoken term discovery systems, and providing several analyses which examine the kinds of structures learned by the model. We also suggest that the ability of the system to successfully unify multiple acoustic sequences into single lexical items relies on the phonological-variability (noisy channel) component of the model—demonstrating the importance of modeling symbolic variation in phonological units. We provide preliminary evidence that simultaneously learning sound and lexical structure leads to synergistic interactions (Johnson, 2008b)—the various components of the model mutually constrain one another such that the linguistic structures learned by each are more accurate than if they had been learned independently.

2 Related Work

Previous models of lexical unit discovery have primarily fallen into two classes: models of spoken term discovery and models of word segmentation. Both kinds of models have sought to identify lexical items from input without direct supervision, but have simplified the joint learning problem discussed in the introduction in different ways.

Spoken Term Discovery Spoken term discovery is the problem of using unsupervised pattern discovery methods to find previously unknown keywords in speech. Most models in this literature have typically made use of a two-stage procedure: First, subsequences of the input that are similar in an acoustic feature space are identified, and, then clustered to discover categories corresponding to lexical items (Park and Glass, 2008; Zhang and Glass, 2009; Zhang et al., 2012; Jansen et al., 2010; Aimetti, 2009; McInnes and Goldwater, 2011). This problem was first examined by Park and Glass (2008) who used Dynamic Time Warping to identify similar acoustic sequences across utterances. The input sequences discovered by this method were then treated as nodes in a similarity-weighted graph, and graph clustering algorithms were applied to produce a number of densely connected groups of acoustic sequences, corresponding to lexical items. Building on this work, Zhang and Glass (2009) and Zhang et al. (2012) proposed robust features that allowed lexical units to be discovered from spoken documents generated by different speakers. Jansen et al. (2010) present a similar framework for finding repeated acoustic patterns, based on line-segment detection in dotplots. Other variants of this approach include McInnes and Goldwater (2011) who compute similarity incrementally, and Aimetti (2009) who integrates a simplified, symbolic representation of visual information associated with each utterance.

Word Segmentation In contrast to spoken term discovery, models of word (or morpheme) segmentation start from unsegmented strings of symbols and attempt to identify subsequences corresponding to lexical items. The problem has been the focus of many years of intense research, and there are a large variety of proposals in the literature (Harris, 1955; Saffran et al., 1996a; Harris, 1955; Olivier, 1968; Saffran et al., 1996b; Brent, 1999b; Frank et al., 2010; Frank et al., 2013). Of particular interest here are models which treat segmentation as a secondary consequence of discovering a compact lexicon which explains the distribution of phoneme sequences in the input (Cartwright and Brent, 1994; Brent, 1999a; Goldsmith, 2001; Argamon et al., 2004; Goldsmith, 2006; Creutz and Lagus, 2007; Goldwater et al., 2009; Mochihashi et al., 2009; Elsner et al., 2013; Neubig et al., 2012; Heymann et al., 2013; De Marcken, 1996c; De Marcken, 1996a). Recently, a number of such models have been introduced which make use of Bayesian nonparametric distributions such as the Dirichlet Process (Ferguson, 1973) or its two-parameter generalization, the Pitman-Yor Process (Pitman, 1992), to define a prior which favors smaller lexicons with more reusable lexical items. The first such models were proposed in Goldwater (2006) and, subsequently, have been extended in a number of ways (Goldwater et al., 2009; Neubig et al., 2012; Heymann et al., 2013;
One important lesson that has emerged from this literature is that models which jointly represent multiple levels of linguistic structure often benefit from synergistic interactions (Johnson, 2008b) where different levels of linguistic structure provide mutual constraints on one another which can be exploited simultaneously (Goldwater et al., 2009; Johnson et al., 2006; Johnson and Demuth, 2010; Johnson and Goldwater, 2009b; Johnson, 2008a; Börschinger and Johnson, 2014; Johnson, 2008b). For example, Elsner et al. (2013) show that explicitly modeling symbolic variation in phoneme realization improves lexical learning—we use a similar idea in this paper.

An important tool for studying such synergies has been the Adaptor Grammars framework of Johnson et al. (2006). Adaptor Grammars are a generalization of Probabilistic Context-free Grammars (PCFGs) which allow the lexical storage of complete subtrees. Using Adaptor Grammars, it is possible to learn lexica which contain stored units at multiple levels of abstraction (e.g., phonemes, onsets, codas, syllables, morphemes, words, and multi-word collocations). A series of studies using the framework has shown that including such additional structure can markedly improve lexicon discovery (Johnson et al., 2006; Johnson and Demuth, 2010; Johnson and Goldwater, 2009b; Johnson, 2008a; Börschinger and Johnson, 2014; Johnson, 2008b). For example, Elsner et al. (2013) show that explicitly modeling symbolic variation in phoneme realization improves lexical learning—we use a similar idea in this paper.

3 Model

3.1 Problem Formulation and Model Overview

Given a corpus of spoken utterances, our model aims to jointly infer the phone-like, sub-lexical, and lexical units in each spoken utterance. To discover these hierarchical linguistic structures directly from acoustic signals, we divide the problem into three sub-tasks: 1) phone-like unit discovery, 2) variability modeling, and 3) sub-lexical and lexical unit learning. Each of the sub-tasks corresponds to certain latent structures embedded in the speech data that our model must identify. Here we briefly discuss the three sub-tasks as well as the latent variables associated with each, and provide an overview on the proposed model for each sub-task.
Figure 1: (a) An overview of the proposed model for inducing hierarchical linguistic structures directly from acoustic signals. As indicated in the graph, the model leverages partial knowledge learned from each level to drive discovery in the others. (b) An illustration of an input example, \( x_i \), and the associated latent structures in the acoustic signals \( d_i \), \( u_i \), \( \alpha_i \), \( \bar{v}_i \), \( z_i \). These latent structures can each be discovered by one of the three components of the model as specified by the red horizontal bars between (a) and (b).

**Phone-like unit discovery** For this sub-task, the model converts the speech input \( x_i \) into a sequence of Phone-Like Units (PLUs), \( \bar{v}_i \), which implicitly determines the phone segmentation, \( z_i \), in the speech data as indicated in (iv)-(vi) of Fig 1-(b). We use \( x_i = \{ x_{i,t} | x_{i,t} \in \mathbb{R}^{39}, 1 \leq t \leq T_i \} \) to denote the series of Mel-Frequency Cepstral Coefficients (MFCCs) representing the \( i^{th} \) utterance (Davis and Mermelstein, 1980), where \( T_i \) stands for the total number of feature frames in utterance \( i \). Each \( x_i \) contains 13-dimensional MFCCs and their first- and second-order time derivatives at a 10 ms frame rate. Each \( x_i \) is also associated with a binary variable \( \bar{z}_{i,t} \), indicating whether a PLU boundary exists between \( x_{i,t} \) and \( x_{i,t+1} \). The feature vectors with \( \bar{z}_{i,t} = 1 \) are highlighted by the dark blue bars in Fig. 1-(vi), which correspond to segment boundaries.

Each speech segment is labelled with a PLU id \( v_{i,j,k} \in \mathbb{L} \), in which \( \mathbb{L} \) is a set of integers that represent the PLU inventory embedded in the speech corpus. We denote the sequence of PLU ids associated with utterance \( i \) using \( \bar{v}_i \) as shown in Fig. 1-(iv), where \( \bar{v}_i = \{ v_{i,j} | 1 \leq j \leq J_i \} \) and \( v_{i,j} = \{ v_{i,j,k} | v_{i,j,k} \in \mathbb{L}, 1 \leq k \leq |v_{i,j}| \} \). The variable \( J_i \) is defined in the discussion of the second sub-task. As depicted in Fig. 1-(a), we construct an acoustic model to approach this sub-problem. The acoustic model is composed of a set of Hidden Markov Models (HMMs), \( \pi \), that are used to infer and model the PLU inventory from the given data.

**Phonological variability modeling** In conversational speech, the phonetic realization of a word can easily vary because of phonological and phonetic context, stress pattern, etc. Without a mechanism that can map these speech production variations into a unique representation, any model that induces linguistic structures based on phonetic input would fail to recognize these pronunciations as instances of the same word type. We exploit a noisy-channel model to address this problem and design three edit operations for the noisy-channel model: substitute, split, and delete. Each of the operations takes a PLU as an input and is denoted as \( \text{sub}(u) \), \( \text{split}(u) \), and \( \text{del}(u) \) respectively. We assume that for every inferred sequence of PLUs \( \bar{v}_i \) in Fig. 1-(b)-(iv), there is a corresponding series of PLUs, \( u_i = \{ u_{i,j} | 1 \leq j \leq J_i \} \), in which the pronunciations for any repeated word in \( \bar{v}_i \) are identical. The variable \( J_i \) indicates the length of \( u_i \). By passing each \( u_{i,j} \) through the noisy-channel model, which stochastically chooses an edit operation \( \alpha_{i,j} \) for \( u_{i,j} \), we obtain the noisy phonetic realization \( \nu_{i,j} \). The relationship among \( u_i \), \( \alpha_i \), and \( \bar{v}_i \) is shown in (ii)-(iv) of Fig. 1-(b). For notation simplicity, we let \( \alpha_{i,j} \) encode \( u_{i,j} \) and \( \nu_{i,j} \), which means we can read \( u_{i,j} \) and \( \nu_{i,j} \) directly from \( \alpha_{i,j} \). We refer to the units that are input to the noisy-channel model \( u_i \) as “top-layer” PLUs and the units that are output from the noisy-channel model \( \bar{v}_i \) as “bottom-layer” PLUs.

\footnote{We denote \( \nu_{i,j} \) as a vector since if a split operation is chosen for \( u_{i,j} \), the noisy-channel model will output two PLUs.}
Sub-word-like and word-like unit learning  With the standardized phone-like representation $u_i$, higher-level linguistic structures can be inferred for each spoken utterance. We employ Adaptor Grammars (AGs) (Johnson et al., 2006) to achieve this goal, and use $d_t$ to denote the parse tree that encodes the hierarchical linguistic structures in Fig. 1-(b)-(i). We bracket sub-word-like (e.g., syllable) and word-like units using [ ] and ( ), respectively.

In summary, our model integrates adaptor grammars with a noisy-channel model of phonetic variability and an acoustic model to discover hierarchical linguistic structures directly from acoustic signals. Even though we have discussed these sub-tasks in a bottom-up manner, our model provides a joint learning framework, allowing knowledge learned from one sub-task to drive discovery in the others. We now a review the formalization of adaptor grammars and define the noisy-channel and acoustic components of our model. We conclude this section by presenting the generative process implied by the three components of our model.

3.2 Adaptor Grammars

Adaptor grammars are a non-parametric Bayesian extension of Probabilistic Context-Free Grammars (PCFGs). A PCFG can be defined as a quintuple $(N, T, R, S, \{\vec{\theta}_q\}_{q \in N})$, which consists of disjoint finite sets of non-terminal symbols $N$ and terminal symbols $T$, a finite set of production rules $R \subseteq \{ N \rightarrow (N \cup T)^* \}$, a start symbol $S \in N$, and vectors of probabilistic distributions $\{\vec{\theta}_q\}_{q \in N}$. Each $\vec{\theta}_q$ contains the probabilities associated with the rules that have the non-terminal $q$ on their left-hand side. We use $\theta_r$ to indicate the probability of rule $r \in R$. We adopt a Bayesian approach and impose a Dirichlet prior on each $\vec{\theta}_q \sim Dir(\vec{\alpha}_q)$.

Let $t$ denote a complete derivation, which represents either a tree that expands from a non-terminal $q$ to its leaves, which contain only terminal symbols, or a tree that is composed of a single terminal symbol. We define $\text{root}(t)$ as a function that returns the root node of $t$ and denote the $k$ immediate subtrees of the root node as $\hat{t}_1, \ldots, \hat{t}_k$. The probability distribution over $T^q$, the set of trees that have $q \in N \cup T$ as the root, is recursively defined as follows.

$$G^q_{\text{pcfg}}(t) = \begin{cases} \sum_{r \in R^q} \theta_r \prod_{i=1}^k G^q_{\text{pcfg}}(\hat{t}_i) \text{ if } \text{root}(t) = q \in N \\ G^q_{\text{pcfg}}(t) = 1 \text{ if } \text{root}(t) = q \in T \end{cases}$$

An adaptor grammar is a sextuple $(N, T, R, S, \{\vec{\theta}_q\}_{q \in N}, \{Y^q\}_{q \in N})$, in which $(N, T, R, S, \{\vec{\theta}_q\}_{q \in N})$ is a PCFG, and $\{Y^q\}_{q \in N}$ is a set of adaptors for the non-terminals. An adaptor $Y^q$ is a function that maps a base distribution over $T^q$ to a distribution over distributions over $T^q$.

The distribution $G^q_{\text{ag}}(t)$ for $q \in N$ of an AG is a sample from this distribution over distributions. Specifically,

$$G^q_{\text{ag}}(t) \sim Y^q(H^q(t))$$

$$H^q(t) = \sum_{r \in R^q} \theta_r \prod_{i=1}^k G^r_{\text{ag}}(\hat{t}_i),$$

where $H^q(t)$ denotes the base distribution over $T^q$. In this paper, following Johnson et al. (2006), we use adaptors that are based on Pitman-Yor processes (Pitman and Yor, 1997). For terminal symbols $q \in T$, we define $G^q_{\text{ag}}(t) = 1$, which is a distribution that puts all its probability mass on the single-node tree labelled $q$. Conceptually, AGs can be regarded as PCFGs with memories that cache the complete derivations of adapted non-terminals, allowing the AG to choose to either reuse the cached trees or select a production an underlying rule in $R$ to expand each non-terminal. For a more detailed description of AGs and their connection to PCFGs, we refer readers to Johnson et al. (2006) and Chapter 3 of O’Donnell (2015).

To discover the latent hierarchical linguistic structures in spoken utterances, we employ the following AG to parse each spoken utterance, where we adopt the notations of Johnson and Goldwater (2009b) and use underlines to indicate adapted non-terminals and employ + to abbreviate right-branching recursive rules for non-terminals. The last rule shows that the terminals of this AG are the PLU ids, which are represented as $u_i$ and depicted as the units in the squares of Fig. 1-(b)-(ii).

Sentence $\rightarrow$ Word$^+$

Word $\rightarrow$ Sub-word$^+$

Sub-word $\rightarrow$ Phone$^+$

Phone $\rightarrow l$ for $l \in \mathbb{L}$

Note that the grammar above only makes use of right-branching rules and therefore could be simulated using finite-state infrastructure, rather than the more complex context-free machinery implicit in the adaptor grammars framework. We nevertheless
make use of the formalism for two reasons. First, on
a theoretical level it provides a uniform framework
for expressing many different assumptions about the
symbolic component of segmentation models (Gold-
water et al., 2009; Johnson, 2008b; Börschinger and
Johnson, 2014; Johnson, 2008a; Johnson and Gold-
water, 2009b; Johnson and Demuth, 2010). Using
adapter grammars to formalize the symbolic compo-
nent our our model thus allows direct comparisons to
this literature as well as transparent extensions fol-
lowing earlier work. Second, on a practical level, us-
ing the framework allowed us to make use of Mark
Johnson’s efficient implementation of the core adap-
tor grammar sampling loop, significantly reducing
model development time.

3.3 Noisy-channel Model

We formulate the noisy-channel model as a PCFG
and encode the substitute, split, and delete oper-
ations as grammar rules. In particular, for \( l \in L \),

\[
\begin{align*}
  l &\rightarrow l' \quad \text{for } l' \in L, \\
  l &\rightarrow l'_1 l'_2 \quad \text{for } l'_1, l'_2 \in L, \\
  l &\rightarrow \epsilon
\end{align*}
\]

(1)

where \( l \in L \) are the start symbols as well as the non-
terminals of the PCFG. The terminals of this PCFG
are \( l' \in L \), which correspond to bottom-layer PLUs
\( \vec{u} \) that are depicted as units in circles in Fig. 1-
(b)-(iv). Note that \{1\} and \{l’\} are drawn from the
same inventory of PLUs, and the notation is meant
to signal that \{l'}\} are the terminal symbols of this
grammar. The three sets of rules respectively map to
the sub(·), split(·), and del(·) operations; thus, the
probability of each edit operation is automatically
aptured by the corresponding rule probability. Note
that to simultaneously infer a phonetic inventory of
an unknown size and model phonetic variation, we
use the infinite PCFG (Liang et al., 2007) to
formulate the noisy-channel model. However, for
computational efficiency, in our experiments, we in-
fer the size of the PLU inventory before training the
full model, and impose a Dirichlet prior on the rule
probability distribution associated with each non-
terminal \( l \). We explain how inventory size is deter-
mined in Sec. 5.2.

3.4 Acoustic Model

Finally, we assign each discovered PLU \( l \in L \) to
an HMM, \( \pi_l \), which is used to model the speech re-
alization of each phonetic unit in the feature space.
In particular, to capture the temporal dynamics of
the features associated with a PLU, each HMM con-
tains three emission states, which roughly corre-
pond to the beginning, middle, and end of a pho-
ett unit (Jelinek, 1976). We model the emission
distribution of each state by using 39-dimensional
diagonal Gaussian Mixture Models (GMMs). The
prior distributions embedded in the HMMs are the
same as those described in (Lee and Glass, 2012).

3.5 Generative Process of the Proposed Model

With the adaptor grammar, the noisy-channel model,
and the acoustic model defined, we summarize the
generative process implied by our model as follows.
For the \( i^{th} \) utterance in the corpus, our model

1. Generates a parse tree \( d_i \) from \( G_{\text{ag}}^{\text{Sentence}}(·) \).

2. For each leaf node \( u_{i,j} \) of \( d_i \), samples an edit
rule \( o_{i,j} \) from \( \vec{\theta}^{u_{i,j}} \) to convert \( u_{i,j} \) to \( v_{i,j} \).

3. For \( v_{i,j,k} \in V_{i,j}, 1 \leq k \leq |V_{i,j}| \), generates the
speech features using \( \pi_{v_{i,j,k}} \), which determinis-
tically sets the value of \( z_{i,t} \).

Thus, the latent variables our model defines
for each utterance are: \( d_i, u_i, o_i, \vec{v}_i, z_i, \pi, \{\vec{\theta}\}_{q \in N_{ag} \cup N_{\text{noisy-channel}}} \). In the next section, we de-
rive inference methods for all the latent variables
except for \( \{\vec{\theta}\}_{q \in N_{ag} \cup N_{\text{noisy-channel}}} \), which we integrate
out during the inference process.

4 Inference

We exploit Markov chain Monte Carlo algorithms
to generate samples from the posterior distribution
over the latent variables. In particular, we construct
three Markov chain kernels: 1) jointly sampling \( d_i, o_i, u_i \), 2) generating new samples for \( \vec{v}_i, z_i \), and 3) updating \( \pi \). Here, we give an overview of each of the
sampling moves.

4.1 Sampling \( d_i, o_i, \) and implicitly \( u_i \)

We employ the Metropolis-Hastings (MH) algo-
ithm (Chib and Greenberg, 1995) to generate sam-
ple for \( d_i \) and \( o_i \), which implicitly determines \( u_i \).
Given $d_{-i}, o_{-i}$, the current parses and the current edit operations associated with all the sentences in the corpus except the $i^{th}$ utterance, we can construct a proposal distribution for $d'_i$ and $o'_i$ by using the approximating PCFG described in Johnson et al. (2006) and the approximated probability of the approximating PCFG described in Johnson et al. (2006) and generate derivations that are rooted at the start symbol of the AG. Therefore, we transform the task of sampling $d'_i$ and $o'_i$ to the task of generating a parse for $\bar{v}_i$ using $G'$, which can be efficiently solved by using an variant of the Inside algorithm for PCFGs (Lari and Young, 1990; Johnson et al., 2007; Goodman, 1998; Finkel et al., 2006).

$$p(d'_i|o_{-i}; \{\bar{a}\}) \approx \frac{C_{-i}(u'_{i,j} \rightarrow v'_{i,j}) + \alpha^w_{d'_i, \rightarrow v'_{i,j}}}{C_{-i}(u'_{i,j}) + \sum_r \alpha^w_{d'_i, \rightarrow v'_{i,j}} \tilde{\alpha}^w_{r, \rightarrow v'_{i,j}}}, \quad (2)$$

where $q \in N_{\text{noisy-channel}}$, and $C_{-i}(w)$ denotes the number of times that $w$ is used in the analyses of the corpus, excluding the $i^{th}$ utterance, in which $w$ can be any countable entity such as a rule or a symbol.

More specifically, we combine the PCFG that approximates the adaptor grammar with the noisy-channel PCFG whose rules are weighted as in Eq. 2 to form a new PCFG $G'$. The new PCFG $G'$ is thus a grammar that can be used to parse the terminals $\bar{v}_i$ and generate derivations that are rooted at the start symbol of the AG. Therefore, we transform the task of sampling $d'_i$ and $o'_i$ to the task of generating a parse for $\bar{v}_i$ using $G'$, which can be efficiently solved by using an variant of the Inside algorithm for PCFGs (Lari and Young, 1990; Johnson et al., 2007; Goodman, 1998; Finkel et al., 2006).

### 4.2 Sampling $\bar{v}_i$ and $z_i$

Given the top-layer PLUs $u_i$ and the speech data $x_i$, sampling the boundary variables $z_i$ and the bottom-layer PLUs $\bar{v}_i$ is equivalent to sampling an alignment between $u_i$ and $x_i$. Therefore, we use the probabilities defined in Eq. 2 and employ the backward message-passing and forward-sampling algorithm described in Lee et al. (2013), designed for aligning a letter sequence and speech signals, to propose samples for $\bar{v}_i$ and $z_i$. The proposals are then accepted by using the standard MH criterion.

### 4.3 Sampling $\pi$

Given $z_i$ and $\bar{v}_i$ of each utterance in the corpus, generating new samples for the parameters of each HMM $\pi_l$ for $l \in L$ is straightforward. For each PLU $l$, we gather all speech segments that are mapped to a bottom-layer PLU $v_{i,j,k} = l$. For every segment in this set, we use $\pi_l$ to block-sample the state id and the GMM mixture id for each feature vector. From the state and mixture assignments, we can collect the counts that are needed to update the priors for the transition probability and the emission distribution of each state in $\pi_l$. New samples for the parameters of $\pi_l$ can thus be yielded from the updated priors.

## 5 Experimental Setup

### 5.1 Dataset

To the best of our knowledge, there are no standard corpora for evaluating models of unsupervised lexicon discovery. In this paper, we perform experiments on the six lecture recordings used in (Park and Glass, 2008; Zhang and Glass, 2009), a part of the MIT Lecture corpus (Glass et al., 2004). A brief summary of the six lectures is listed in Table 1.

| Lecture topic            | Duration |
|--------------------------|----------|
| Economics                | 75 mins  |
| Speech processing        | 85 mins  |
| Clustering               | 78 mins  |
| Speaker adaptation       | 74 mins  |
| Physics                  | 51 mins  |
| Linear algebra           | 47 mins  |

Table 1: A brief summary of the six lectures used for the experiments reported in Section 6.

### 5.2 Systems

**Full system** We constructed two systems based on the model described in Sec. 3. These systems, FullDP and Full50, differ only in the size of the PLU inventory ($K$). For FullDP, we set the value of $K$ to be the number of PLUs discovered for each lecture by the DPHMM framework presented in (Lee and Glass, 2012). These numbers were: Economics, 99; Speech Processing, 111; Clustering, 91; Speaker Adaptation, 83; Physics, 90; and Algebra, 79. For Full50, we used a fixed number of PLUs, $K = 50$.

The acoustic component of the FullDP system was initialized by using the output of the DPHMM model for each lecture. Specifically, we made use of the HMMs, the phone boundaries, and the PLU that the DPHMM model found as the initial values for $\pi$, $z_i$, and $\bar{v}_i$ of the FullDP system. After initialization, the training of FullDP proceeds by following...
the three sampling moves described in Sec. 4. Similarly, we employ a Hierarchical HMM (HHMM), which is presented in detail in (Lake et al., 2014), to find the initial values of $\pi$, $z_i$, and $\bar{v}_i$ for the Full50 system. The adaptor grammar component of all systems was initialized following the “batch initialization” method described in Johnson and Goldwater (2009b) which independently samples an AG analysis for each utterance. The lesioned systems that are described in the rest of this section were also initialized in the same manner.

To reduce the inference load on the HMM, we exploit acoustic cues in the feature space to constrain phonetic boundaries to occur at a subset of all possible locations (Lee and Glass, 2012). We follow the pre-segmentation method described in (Glass, 2003) to achieve the goal. Empirically, this boundary elimination heuristic reduces the computational complexity of the inference algorithm by roughly an order of magnitude on clean speech corpora.

No acoustic model We remove the acoustic model from FullDP and Full50 to obtain the -AM systems. Since the -AM systems do not have an acoustic model, they cannot resegment or relabel the data, which implies that there is no learning of phonetic units in the -AM systems, making them similar to symbolic segmentation models that include a noisy channel component (Elsner et al., 2013). By comparing a -AM system to its full counterpart, we can investigate the synergies between phonetic and lexical unit acquisition in the full model.

No noisy-channel To evaluate the importance of modeling phonetic variability, we remove the noisy-channel model from the -AM systems to form -NC systems. A -NC system can be regarded as a pipeline, whereby utterance phone sequences are discovered first, and latent higher-level linguistic structures are learned in the second step and thus is similar to models such as that of Jansen et al. (2010).

6 Results and Analyses

Training convergence Fig. 2 shows the negative log posterior probability of the sampled parses $d$ and edit operations $o$ for each lecture as a function of iteration generated by the FullDP system. Given that each lecture consists of roughly only one hour of speech data, we can see that the model converges fairly quickly within a couple hundreds of iterations. In the this section, we report the performance of each system using the corresponding sample from the 200th iteration.

Phoneme segmentation We first evaluate our model on the task of phone segmentation for the six lectures. We use a speech recognizer to produce phone forced alignments for each lecture. The phone segmentation embedded in the forced alignments is then treated as the gold standard to which we compare the segmentation our model generates. We follow the suggestion of (Scharenborg et al., 2010) and use a 20-ms tolerance window to compute the F1 score of all proposed phone segmentations.

Table 2 presents the F1 scores achieved by different systems. Because the -AM and -NC systems do not do inference over acoustic segmentations, we compare the phoneme-segmentation performance of each full system to its performance at initialization. Recall that the Full50 system is initialized using the output of a Hierarchical HMM (HHMM), and the FullDP system is initialized using DPHMM.

From Table 2 we can see that the two -AM systems achieve roughly the same segmentation performance for the first four lectures. Aside from using the boundary elimination method described in (Lee and Glass, 2012), these two systems are trained independently. The table shows that the two initialization systems achieve roughly the same segmentation
| Lecture topic  | Full50 | HHMM | FullDP | DPHMM |
|---------------|--------|------|--------|-------|
| Economics     | 74.4   | 74.6 | 74.6   | 75.0  |
| Signal processing | 76.2   | 76.0 | 76.0   | 76.3  |
| Clustering    | 76.6   | 76.6 | 77.0   | 76.9  |
| Speaker adaptation | 76.5   | 76.9 | 76.7   | 76.9  |
| Physics      | 75.9   | 74.9 | 75.7   | 75.8  |
| Linear algebra | 75.5   | 73.8 | 75.5   | 75.7  |

Table 2: The F1 scores for the phone segmentation task obtained by the full systems and their corresponding initialization systems.

| Lecture topic  | Full50 | -AM | -NC | FullDP | -AM | -NC |
|---------------|--------|-----|-----|--------|-----|-----|
| Economics     | 15.4   | 15.4| 14.5| 16.1   | 14.9| 13.8|
| Signal processing | 17.5   | 16.4| 12.1| 18.3   | 17.0| 14.5|
| Clustering    | 16.7   | 18.1| 15.9| 18.4   | 16.9| 15.2|
| Speaker adaptation | 17.3   | 17.4| 15.4| 18.7   | 17.6| 16.2|
| Physics      | 17.7   | 17.9| 15.6| 20.0   | 18.0| 15.2|
| Linear algebra | 17.9   | 17.5| 15.4| 20.0   | 17.0| 15.6|

Table 3: F1 scores for word segmentation obtained by the full systems and their ablated systems.

performance for the first four lectures. Thus, their narrow performance gap indicates that the two initialization systems may have already found a near-optimal segmentation.

Since our model also looks for the best segmentation in the same hypothesis space, by initializing the boundary variables around the optimum, our model should simply maintain the segmentation. In particular, as shown in Table 2, the full systems also achieve about the same performance as the -AM systems for the first four lectures, with the overall largest performance difference being 0.4%.

It is perhaps more interesting when the initialization system gets stuck at a local optimum. By comparing the performance of the two -AM systems for the last two lectures, we can see that the initialization of Full50 converges to local optima for the two lectures. Nonetheless, as shown in Table 2, the Full50 system is able to improve the given initial segmentation and reach a similar performance to that accomplished by the FullDP and the initialization of the FullDP systems.

**Word segmentation** In addition to phone segmentation, we also evaluate our model on the task of word segmentation. Similar to how we generate the gold standard segmentation for the previous task, we use a speech recognizer to produce word alignments and obtain the word segmentation for each lecture. We then compare the word segmentation that our systems generate to the gold standard and calculate the F1 scores by using a 20-ms tolerance window.

By comparing the full systems to their -NC counterparts, we can see that the noisy-channel model plays an important role for word segmentation, which resonates with the findings of in (Elsner et al., 2013). Without the capability of modeling phonetic variability, it is difficult, or even impossible, for the -NC systems to recognize word tokens of the same type but with different phonetic realizations.

We can also observe the advantage of joint learning both word-level and phone-level representations by comparing the FullDP system to the corresponding -AM model. On average, the FullDP system outperforms its -AM ablated counterpart by 1.6% on the word segmentation task, which indicates that the top-down word-level information can help refine the phone-level knowledge that the model has learned.

While similar improvements are only observed in two lectures for the Full50 and its -AM version, we believe it’s because the Full50 system does not have as much flexibility to infer the phonetic embeddings as the FullDP system. This inflexibility may have
Table 4: The number of the 20 target words discovered by each system described in Sec. 5, and by the baseline (Park and Glass, 2008), and state-of-the-art system (Zhang, 2013). The best performance achieved for each lecture is shown in bold.

| Lecture topic     | Full50 | -AM | -NC | FullDP | -AM | -NC | P&G 2008 | Zhang 2013 |
|-------------------|--------|-----|-----|--------|-----|-----|---------|-----------|
| Economics         | 12     | 4   | 2   | 12     | 9   | 6   | 11      | 14        |
| Signal processing | 16     | 16  | 5   | 20     | 19  | 14  | 15      | 19        |
| Clustering        | 18     | 17  | 9   | 17     | 18  | 13  | 16      | 17        |
| Speaker adaptation| 14     | 14  | 8   | 19     | 17  | 13  | 13      | 19        |
| Physics           | 20     | 14  | 12  | 20     | 18  | 16  | 17      | 18        |
| Linear algebra    | 18     | 16  | 11  | 19     | 17  | 7   | 17      | 16        |

prevented the Full50 system to fully exploit the top-down information for learning.

Finally, note that even though the F1 scores for the word segmentation task are low, we find similar performance reported in Jansen et al. (2013). We would like to raise the question of whether the conventional word segmentation task is a proper evaluation method for an unsupervised model such as the one described in this paper. Our thought is two fold. First, correct segmentation is vaguely defined. By choosing different tolerance windows, different segmentation performance is obtained. Second, as we show later, many of the units discovered by our model are linguistically meaningful, although they do not always strictly correspond to words (i.e., the units may be morphemes or collocations, etc.). Since these are linguistically meaningful units which should be identified by an unsupervised lexical discovery model, it is not clear what advantage would be gained by privileging words in the evaluation. Nevertheless, we present the word segmentation performance achieved by our model in this paper for future references.

Coverage of words with high TFIDF scores To assess the performance of our model, we evaluate the degree to which it was able to correctly recover the vocabulary used in input corpora. To facilitate comparison with the baseline (Park and Glass, 2008) and state-of-the-art (Zhang, 2013) spoken term discovery systems, we restrict attention to the top 20 highest TFIDF scoring words for each lecture. Note that the set of target words of each lecture were originally chosen in (Park and Glass, 2008) and used as the evaluation set in both Park and Glass (2008) and Zhang (2013). To compare our system directly to previous work, we use the same set of target words to test our model.3

Table 4 summarizes the coverage achieved by each variant of our model as well as the two spoken term discovery systems. Note that these two systems differ only in the acoustic features used to represent the input: MFCC features versus more robust Gaussian posteriorgrams, respectively. Both the FullDP and Full50 systems consistently outperform the baseline. Both systems also exceed or perform as well as the state-of-the-art system on most lectures. Furthermore, they do so using the less robust MFCC feature-based acoustic representation.

The results in Table 4 also illustrate the synergistic interactions that occur between the acoustic and symbolic model components. As described in Sec. 5, the -AM systems are identical to the full systems, except they do not include the acoustic model, and, therefore, do not re-segment or relabel the speech after initialization. As Table 4 shows, the Full50 and FullDP models both tend to have coverage which is as good as, or better than, the corresponding models without an acoustic component. This indicates that top-down pressure from the symbolic component can refine bottom-layer PLUs, leading, ultimately, to better lexicon discovery.

Finally, the comparison between Full/-AM models and their -NC components suggests the importance of modeling variability in the realization of phonemes. As we will discuss in the next section, the full model tends to merge multiple sequences of

3For the procedure used to identify the word label for each lexical unit, we refer the reader to Sec. 3.5.3 of (Lee, 2014) for detailed explanation.
Figure 3: The bottom-layer PLUs \( \vec{v} \) and the top-layer PLUs \( u \) as well as the word-internal structure that the FullDP system discovered for three instances of the words (a) globalization and (b) collaboration. We also include phoneme transcriptions (derived by manual inspection of spectrograms), for clarity.

bottom-layer PLUs into single lexical items which share a single top-layer PLU sequence. The results in Table 4 confirm this: When the model does not have the option of collapsing bottom-layer PLU sequences, word discovery degrades considerably.

Examples and qualitative analyses To provide intuition about the model behavior, we present several examples and qualitative analyses. Figure 3 illustrates the model’s representation of two words which appeared frequently in the economics lecture: globalization and collaboration. The figure shows (i) the bottom-layer PLUs which the model assigned to three instances of each word in the training corpus, (ii) the alignments between these bottom-layer PLUs and the top-layer PLU sequence corresponding the model’s lexical representation of each word, (iii) the decomposition of each word-like unit into sub-word-like units, which are denoted as bracketed sequences of PLUs (e.g., \([70 \ 110 \ 3]\)), and (iv) a hand annotated phonemic transcription.

The first thing to note is the importance of the noisy-channel component in normalizing variation across word tokens. In Figure 3-(a) the model has inferred a different sequence of bottom-layer PLUs for each spoken instance of globalization. PLUs which vary between the three instances are highlighted in red. The model was able to map these units to the single sequence of top-layer PLUs associated with the lexical item. Similar remarks hold for the word collaboration in Figure 3-(b). This suggests that acoustic variability between segments led the model to infer different bottom-layer PLUs between word tokens, but this variability was correctly normalized by the noisy-channel component.

The second thing to note is the large amount of variability in the granularity of stored sub-word-like units (bracketed PLU sequences). The model allows sub-word-like units to consist of any sequence of PLUs, without further constraint. Figure 3 shows that the model makes use of the flexibility, representing linguistic structure at a variety of different scales. For example, the initial sub-word-like unit of collaboration groups together two PLUs corresponding to a single phoneme /k/. Other sub-word-like units correspond to syllables. Still others capture morphological structure. For example, the final sub-word-like unit in both words (highlighted in green) corresponds to the combination of suffixes -ation—a highly productive unit in English (O’Donnell, 2015).  

\[\text{The reader may notice that the lexical representations are missing a final /n/ phoneme. Manual examination of spectro-}\]
Table 5: A subset of the lexical units that the FullDP system discovers for the economics lecture. The number of independent speech segments that are associated with each lexical unit is denoted as |Word|.

Lexical units also exhibit variability in granularity. Table 5 shows a subset of lexical units discovered by the FullDP system for the economics lecture. Each entry in the table shows (i) the decomposition of each word-like unit into sub-word-like units, (ii) a phonemic transcription of the unit, and (iii) the number of times each lexical unit was used to label a segment of speech in the lecture (denoted as |Word|). The lexical units displayed in the table correspond, for the most part, to linguistic units. While there are a few cases, such as /iy l iy/, where the model stored a sequence of phones which does not map directly onto a linguistic unit such as a syllable, morpheme, or word, most stored units do correspond to intuitively plausible linguistic constituents.

However, like sub-word-like units, there is variability in the scale of the linguistic structure which they capture. On one hand, the model stores a number of highly reusable smaller-than-word units, which typically correspond to morphemes or highly frequent syllables. For example, the sequences /ax bcl ax l/ and /ey sh ax n/ correspond to the productive suffix -able and suffix combination -ation (O’Donnell, 2015). On the other hand, the model also stores lexical units which correspond to words (e.g., powerful) and multi-word collocations (e.g., the arab muslim world). Figure 4 shows an analysis of stored lexical units for each lecture, plotting the proportion of stored items which map onto sub-words, words, and multi-word collocations for each.

Why does the model choose to store some units and not others? Like many approaches to lexicon learning (Goldwater, 2006; De Marcken, 1996c; Johnson et al., 2006), our model can be understood as balancing a tradeoff between productivity (i.e., computation) and reuse (i.e., storage). The model attempts to find a set of lexical units which explain the distribution of forms in the input, subject to two opposing simplicity biases. The first favors smaller numbers of stored units. The second favors derivations of observed utterances which use fewer computational steps (i.e., using small number of lexical items). Storing larger lexical units, like the arab muslim world, leads to simpler derivations of individual utterances, but a larger lexicon. Storing smaller lexical units, like the suffix -able, leads to a more compact lexicon, but more complex derivations individual utterances.
Smaller units are favored when they are used across a large variety of relatively infrequent contexts. For example, -ation appears in a large number of input utterances, but often as part of words which themselves are relatively infrequent (e.g., conversation, reservation, innovation, and foundation which appear 2, 3, 4, and 2 times respectively). Larger units will be favored when a combination of smaller units appears more frequently than would be predicted by considering their probabilities in isolation. For example, the model stores the words globalization and collaboration in their entirety, despite also storing the suffix combination -ation. These words occur 25 and 21 times respectively in the lecture, which is a greater number of times than would be expected merely by considering the words sub-parts. Thus, the fact that the model stores a variety of lexical units at different granularities is expected.

7 Conclusion and Future Work

In this paper, we have presented a probabilistic framework for inferring hierarchical linguistic structures from acoustic signals. Our approach is formulated as an integration of adaptor grammars, a noisy-channel model, and an acoustic model. Comparison of the model with lesioned counterparts suggested that our model takes advantage of synergistic interactions between phonetic and lexical representations. The experimental results also indicate that modeling phonetic variability may play a critical role in inferring lexical units from speech.

While the noisy-channel model has demonstrated an ability to normalize phonetic variations, it has its limitations. In the future, we plan to investigate alternatives that more accurately capture phonetic variation. We also plan to explore grammars that encode other types of linguistic structures such as collocation of lexical and morphological units.

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