The rise of grasslands is linked to atmospheric CO$_2$ decline in the late Palaeogene

Supporting Information

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S1  Taxonomic representativeness of the most important vascular plant families in grasslands

Figure S1: Taxonomic representativeness of the most important vascular plant families in grasslands. We selected seven WWF open-habitat eco-regions and quantified the number of species of the most abundant families using the R package ‘rgbif’ [5].
Figure S2: Extent of major biomes (107 km²) using an equilibrium vegetation model (BIOME4) [9]. a) Intertropical (30°N-30°S) extent of tropical forest, savanna and dry woodland, desert, grassland and dry shrubland and warm-temperate forest as a result of simulated LGM climate changes alone, LGM climate and reduced CO₂ concentrations compared to modern extent of the same biomes. b) Northern hemisphere extent of tundra, boreal-temperate forest, desert and grassland and dry shrubland as a result of simulated LGM climate changes alone, LGM climate plus reduced CO₂ conditions. The output of each of the seventeen climate simulations was averaged for each major biome in order to obtain a more compelling story about the effects of climate and CO₂ concentrations on the vegetation. Overall, the modeled physiological impact of low CO₂ produces i) a pronounced shift towards open-habitat vegetation, and ii) a reduction of ~50% of reduction in the area of tropical forests compared to the area simulated under modern climate and CO₂ conditions [9].
S3  Asteraceae fossil species

Table S1: Asteraceae fossil species. Fossil data from Asteraceae come almost exclusively from pollen grains. The oldest Asteraceae-like pollen comes from the latest Cretaceous of Antarctica and New Zealand [3], assigned to the Barnadesioideae, the sister subfamily to the core-Asteraceae. The unique macrofossil (florestes and associated pollen grains) confidently assigned to Asteraceae comes from the Middle Eocene of Patagonia showing similarities with the Mutisioideae and Carduoideae [2]. The earliest record of the Asteraceae (the clade that includes the most common open-habitat daisy tribes) occurs since the Late Oligocene of New Zealand but in very low frequencies. Fossils refer to this subfamily increased in abundance and diversity during the Miocene and Pliocene. Pollen referred to Artemisia, in particular, did not become abundant until the Middle-Late Miocene with several reports from central Europe, Asia and North America. Pre-Miocene findings need further verification. Overall, the Late Oligocene and in particular the Miocene witnessed the major step on the diversification of Asteraceae; ca. 80% of the fossil species recorded have been defined for this time interval.

| Species | Botanical Affinity | Epoch |
|---------|--------------------|-------|
| Tubulifloridites lilliei type A sensu Barreda et al | Barnadesioideae | Maastrichtian |
| Tubulifloridites sp. sensu Raine 2008 | Mutisioideae/Carduoideae? | Early Eocene |
| Mutisapollis telleri Barreda and Palazzesi | Mutisioideae/Carduoideae | Middle Eocene |
| Mutisapollis sp. Barreda et al | Mutisioideae/Carduoideae | Miocene/Pliocene |
| Mutisapollis patersonii Macphail and Hill | Mutisioideae (Mutisieae, Mutisia type) | Early Miocene |
| Tubulifloridites antipodica Cookson | Asteroideae | Oligocene/Miocene |
| Tricolporopollenites microechinatus Trevisan | Asteroideae | Oligocene/Miocene |
| Mutisapollis vitoanus Barreda | Gochnatioideae (Cnicothamnus type) | Miocene |
| Huanilipollis cabrerii Barreda and Palazzesi | Mutisioideae (Nassauvieae) | Miocene |
| Huanilipollis criscii Barreda and Palazzesi | Mutisioideae (Nassauvieae) | Miocene |
| Cichorieacidites xeroxformis Zheng | Cichorioidae | Miocene |
| Lapsona type Luncucks-Srodoniowa | Cichorioidae (Cichorieae) | Miocene |
| Tubulifloridites grumulosus Nagy | Asteroideae | Miocene |
| Tubulifloridites simplis Martin | Asteroideae | Miocene |
| Echitricolporites spinosus Germeraad et al | Asteroideae | Miocene |
| Tubulifloridites anthemidearum Nagy | Asteroideae (Anthemideae) | Miocene |
| Artemasia type sensu Leopold | Asteroideae (Anthemideae) | Miocene |
| Tubulifloridites ambrosiniae Nagy | Asteroideae (Ambrosiinae) | Miocene |
| Tubulifloridites sp. (Ambrosia type) Guler et al | Asteroideae (Heliantheae) | Miocene |
| Xanthium type Cavallo and Martinetto | Asteroideae (Heliantheae) | Miocene |
| Tubulifloridites grandis Nagy | Asteroideae? | Miocene |
| Compositae indet sensu Graham | Asteroideae? | Miocene |
| Quilembaypollis gamerro Barreda and Barreda | Barnadesioideae (Chuquiraga type) | Miocene |
| Quilembaypollis sasseyi Barreda and Barreda | Barnadesioideae (Dasyphyllum type) | Miocene |
| Quilembaypollis sasseyi Barreda and Barreda | Barnadesioideae (Schlechsteinia type) | Miocene |
| Cirsium type Luncucks-Srodoniowa | Carduoideae | Miocene |
| Cichoriceparapollenites gracilis Nagy | Cichorioidae | Miocene |
| Cichorium intybus type Hochuli | Cichorioidae (Cichorieae) | Miocene |
| Mutisapollis sp. sensu Barreda et al 2006 | Cichorioidae (Cichorieae, Artemisia type) | Miocene/Pliocene |
| Tricolporopollenites ratispinulitellatus Trevisan | Asteroideae (Anthemideae, Artemisia type) | Miocene/Pliocene |
| Tricolporopollenites varispinaulitellatus Trevisan | Asteroideae (Anthemideae) | Miocene/Pliocene |
| Artemisaaecapollenites minor Zhu | Asteroideae (Anthemideae) | Miocene/Pliocene |
| Tubulifloridites minutus Regali | Asteroideae (Anthemideae, Soldago type) | Miocene/Pliocene |
| Echitricolporites mceoniliiy Germeraad et al | Asteroideae (Heliantheae, Ambrosiinae) | Miocene/Pliocene |
| Echitricolporites sp. sensu Wang | Asteroideae | Miocene/Pliocene |
| Tubulifloridites sp. sensu Wang | Asteroideae? | Miocene/Pliocene |
| Tricolporopollenites kazemiensis Weiland | Carduoideae? | Miocene/Pliocene |
| Tubulifloridites macrochinitus Nagy | Carduoideae? | Miocene/Pliocene |
| Tricolporopollenites macrospinaulitellatus Trevisan | Cichorioidae (Cichorieae, Sonchus type) | Miocene/Pliocene |
| Cichoroideae type sensu Blackmore | Cichorioidae (Cichorieae) | Miocene/Pliocene |
| Penestrites longispinosus Lorente | Cichorioidae (Cichorieae) | Miocene/Pliocene |
| Liquifloridites sp. sensu Couper | Cichorioidae (Cichorieae) | Miocene/Pliocene |
| Sonchus type sensu Blackmore | Cichorioidae (Cichorieae) | Pliocene |
| Penestrites spinosus Hammen | Cichorioidae (Cichorieae/Vernoniae) | Pliocene |
| Artemisaaecapollenites sellulars Nagy | Asteroideae (Anthemideae) | Pliocene |
| Artemisaaecapollenites leatus Zheng | Asteroideae (Anthemideae) | Pliocene |
| Scorzonera type sensu Blackmore | Asteroideae (Anthemideae) | Pliocene |
| Tubulifloridites pleistocenius Martin | Asteroideae | Pliocene/Pleistocene |
## S4  Asteraceae genes

Table S2: Asteraceae genes Number of taxa (total and sampled) and genes used in phylogenetic analyses for each clade of Asteraceae.

| Clades           | Number of Species | Sampled Species | Age  | Genes                                                                 |
|------------------|-------------------|-----------------|------|----------------------------------------------------------------------|
| Barnadesioideae  | 92                | 70              | 64.41| ITS, trnL, matK except 7 species of the backbone that include 12 markers (see Panero et al. 2015) |
| Famatinanthoideae| 1                 | 1               | 60.82| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon2, trnL intron-trnL-F spacer |
| Mutisioideae     | 637               | 210             | 40.55| ITS, ndhF except 12 species of the backbone that include 12 markers |
| Stifftioideae    | 35                | 4               | 34.84| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Wunderlichioideae| 48                | 6               | 48.88| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Gochnatioideae   | 85                | 32              | 42.60| ndhF, trnL except 3 species of the backbone that include 12 markers |
| Hecastocleidoideae| 1                | 1               | 46.86| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Caruroideae      | 2865              | 373             | 24.26| psbA-trnH, matK except 5 species of the backbone that include 12 markers |
| Gymnarrhoideae   | 2                 | 1               | 38.19| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Corymbioideae    | 7                 | 1               | 32.13| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Inuleae          | 680               | 105             | 20.03| psbA-trnH, trnL-F except 1 species of the backbone that include 12 markers |
| Helianthodae     | 6611              | 510             | 21.41| ITS, matK except 6 species of the backbone that include 12 markers |
| Senecionodae-Asterodae | 10589   | 648             | 26.60| ITS, trnL-trnF except 3 species of the backbone that include 12 markers |
| Cichorioideae    | 3994              | 759             | 28.51| ITS, trnL-trnF except 4 species of the backbone that include 12 markers |
| Pertyoideae      | 70                | 2               | 17.35| accD, atpB, matK, ndhD, ndhF, ndhI, ndhJKC, rbcL, rpoB, rpoC1 exon1, rpoC1 exon2, trnL intron-trnL-F spacer |
| Total            | 25717             | 2723            |      |                                                                      |
### S5  Poaceae genes

**Table S3: Poaceae genes** Number of taxa (total and sampled) and genes used in phylogenetic analyses for each clade of Poaceae according to Spriggs et al (2014). Age estimations correspond to the calibration scenario 1 of Spriggs et al (2014) [17]

| Clades                  | Number of Species | Sampled Species | Age   | Genes                                                                 |
|-------------------------|-------------------|-----------------|-------|----------------------------------------------------------------------|
| Pharoideae              | 12                | 1               | 57.80 | matK, ndhF, rbcL                                                     |
| Puelioideae             | 11                | 1               | 53.98 | matK, ndhF, rbcL                                                     |
| Ehrhartioideae          | 112               | 66              | 33.77 | GPA1, ITS, matK, ndhC, ndhF, psbHpetB, psbZ, rbcL, rps19, trnHpsbA, ycf3 |
| Bambusoideae            | 1441              | 418             | 23.27 | matK, ndhF, rbcL, ITS, psbA-trnH, rpl16, rpl32, rps16-trnQ, trnC-rpoB, trnL-trnF, trnTtrnD |
| Pooideae                | 3850              | 1335            | 38.25 | DMC1, ITS, matK, ndhF, pgk1, psbAtrnH, rbcL, rps2, rpoA, rps19, trnKtrp16, trnLtrnF |
| Aristidoideae           | 365               | 125             | 27.95 | ITS, matK, ndhF, rbcL, rpl16, trnL-trnF                               |
| Centothecae             | 33                | 33              | 29.66 | ndhF, rbcL, matk, trnLtrnF, phyB, ITS                               |
| Andropogoneae           | 1274              | 250             | 16.97 | ITS, phyB, trnLtrnF, matK, ndhF, rbcL                               |
| Paspaleae               | 664               | 168             | 21.01 | trnL-trnF, rbcL, psbA-trnH, atpB-rbcL, trnG, rpl16, ndhF, matK, ITS  |
| Panicoideae-Gynieae     | 1254              | 387             | 21.29 | ITS, kn1, matK, ndhF, rbcL, rpl16, trnLtrnF                          |
| Danthonioideae          | 281               | 234             | 28.71 | ndhF, rbcL, atpB-rbcL, ITS, psbM, rpl16, rpoC2, trnC-trnD, trnL, ycf6-trnC, trnT-trnL, matK |
| Chloridoideae           | 1721              | 534             | 32.91 | ITS, matK, ndhF, rbcL, rps16, rpl3, trnL-trnF                         |
| Arundinoideae-Micrairoideae | 188+46         | 43              | 30.38 | ITS, rpoC2, matK, ndhF, rbcL                                      |
| Total                   | 11256             | 3595            |       |                                                                       |
Figure S3: Environmental CO$_2$ and changes in CO$_2$ between time intervals. The lighter green line shows the environmental CO$_2$ as was used in the environmentally-dependent diversification rates models. The darker green line shows the changes in CO$_2$ over time, which might translate into changes in diversification rates if diversification rates are correlated with environmental CO$_2$. 
S7  Models and Priors for the environmental correlation analyses

S7.1  Fixed

Our first model, which is equivalent to the exponential environmentally-dependent diversification model of Condamine et al. [6], has two parameters per speciation and extinction rate; the initial rate \( \lambda_0 \) and \( \mu_0 \) and the correlation factor \( \beta \), with

\[
\begin{align*}
\lambda_0 & \sim \text{Uniform}(0, 100) \\
\ln(\lambda_i) &= \ln(\lambda_{i-1}) + \beta \lambda \times \Delta CO_2 \\
\ln(\mu_i) &= \ln(\mu_{i-1}) + \beta \mu \times \Delta CO_2
\end{align*}
\]

(S1)

(S2)

Table S4: Model parameter names and prior distributions for the fixed model.

| Parameter                        | \( X \)     | \( f(X) \) |
|----------------------------------|-------------|-------------|
| Speciation at present \( \lambda_0 \) | Uniform(0,100) |             |
| Extinction at present \( \mu_0 \)     | Uniform(0,100) |             |
| Speciation Correlation \( \beta_\lambda \) | Normal(0,1) |             |
| Extinction Correlation \( \beta_\mu \)   | Normal(0,1) |             |

S7.2  UC

The second model extends our first model by additional “errors”, or variation, on top of the diversification rate variation due to the environmental variable. Thus, we additionally have a variance parameter \( \sigma^2 \) as well as \( \epsilon_\lambda \) and \( \epsilon_\mu \) per interval. The resulting speciation and extinction rates are computed by

\[
\begin{align*}
\lambda_0 & \sim \text{Uniform}(0, 100) \\
\ln(\hat{\lambda}_i) &= \ln(\hat{\lambda}_{i-1}) + \beta \lambda \times \Delta CO_2 \\
\sigma & \sim \text{halfCauchy}(0,1) \\
\epsilon_i & \sim \text{Normal}(0, \sigma) \\
\ln(\hat{\lambda}_i) &= \ln(\hat{\lambda}_i) + \epsilon_i
\end{align*}
\]

(S3)

(S4)

(S5)

(S6)

(S7)

Table S5: Model parameter names and prior distributions for the UC model.

| Parameter                        | \( X \)     | \( f(X) \)   |
|----------------------------------|-------------|---------------|
| Speciation at present \( \lambda_0 \) | Uniform(0,100) |             |
| Extinction at present \( \mu_0 \)     | Uniform(0,100) |             |
| Speciation Variation \( \sigma_\lambda \) | HalfCauchy(0,1) |          |
| Extinction Variation \( \sigma_\mu \)   | HalfCauchy(0,1) |             |
| Speciation Correlation \( \beta_\lambda \) | Normal(0,1) |          |
| Extinction Correlation \( \beta_\mu \)   | Normal(0,1) |             |
| Per interval log-speciation rate variation \( \epsilon_\lambda \) | Normal(0,\( \sigma_\lambda \)) |              |
| Per interval log-extinction rate variation \( \epsilon_\mu \)   | Normal(0,\( \sigma_\mu \)) |             |
S7.3 Gaussian Markov Random Field (GMRF)

The GMRF model has autocorrelated rate variation compared to the uncorrelated variation from the UC model. The speciation and extinction rates are computed by

\[
    \lambda_0 \sim \text{Uniform}(0, 100) \quad (S8)
\]
\[
    \sigma \sim \text{halfCauchy}(0, 1) \quad (S9)
\]
\[
    \epsilon_i \sim \text{Normal}(0, \sigma) \quad (S10)
\]
\[
    \ln(\lambda_i) = \ln(\lambda_{i-1}) + \beta_\lambda \times \Delta CO_2 + \epsilon_i \quad (S11)
\]

We additionally used a global scaling parameter for the variation of diversification of \( \zeta = 0.587405 \times N \), where \( N \) is the number of epochs, so that we expect one order of magnitude variation over the course of the age of the phylogeny [15]. Alternatively, the parameter \( \zeta \) could be place into the prior distribution on \( \sigma \) by using a \text{halfCauchy}(0, \zeta) prior distribution instead. Both approaches are equivalent.

Table S6: Model parameter names and prior distributions for the GMRF model.

| Parameter                  | Name       | Distribution               |
|----------------------------|------------|---------------------------|
| Speciation at present      | \( \lambda_0 \) | Uniform(0,100)            |
| Extinction at present      | \( \mu_0 \) | Uniform(0,100)            |
| Speciation Variation       | \( \gamma_\lambda \) | HalfCauchy(0,1)           |
| Extinction Variation       | \( \gamma_\mu \) | HalfCauchy(0,1)           |
| Speciation Correlation     | \( \beta_\lambda \) | Normal(0,1)               |
| Extinction Correlation     | \( \beta_\mu \) | Normal(0,1)               |
| Per interval log-speciation rate difference | \( \ln(\Delta \lambda) \) | Normal(0,\( \gamma_\lambda \zeta \)) |
| Per interval log-extinction rate difference | \( \ln(\Delta \mu) \) | Normal(0,\( \gamma_\mu \zeta \)) |

S7.4 HSMRF

The HSMRF model allows for interval specific variance parameters \( \gamma_i^2 \). This allows for some epochs to be more variable, while most epochs will actually be less variable [15]. The resulting speciation and extinction rates are thus computed by

\[
    \lambda_0 \sim \text{Uniform}(0, 100) \quad (S12)
\]
\[
    \sigma \sim \text{halfCauchy}(0, 1) \quad (S13)
\]
\[
    \gamma_i \sim \text{halfCauchy}(0, 1) \quad (S14)
\]
\[
    \epsilon_i \sim \text{Normal}(0, \sigma_i \zeta) \quad (S15)
\]
\[
    \ln(\lambda_i) = \ln(\lambda_{i-1}) + \beta_\lambda \times \Delta CO_2 + \epsilon_i \quad (S16)
\]

As before, we additionally used a global scaling parameter for the variation of diversification of \( \zeta = 0.587405 \times N \) so that we expect one order of magnitude variation over the course of the age of the phylogeny [15].
Table S7: Model parameter names and prior distributions for the HSMRF model.

| Parameter                                      | X          | f(X)          |
|------------------------------------------------|------------|---------------|
| Speciation at present                         | $\lambda_0$ | Uniform(0,100) |
| Extinction at present                         | $\mu_0$    | Uniform(0,100) |
| Speciation Variation                          | $\sigma_\lambda$ | HalfCauchy(0,1) |
| Extinction Variation                          | $\sigma_\mu$ | HalfCauchy(0,1) |
| Speciation Correlation                        | $\beta_\lambda$ | Normal(0,1) |
| Extinction Correlation                        | $\beta_\mu$ | Normal(0,1) |
| Per interval speciation rate variation factor | $\gamma_{\lambda,i}$ | HalfCauchy(0,1) |
| Per interval extinction rate variation factor | $\gamma_{\mu,i}$ | HalfCauchy(0,1) |
| Per interval log-speciation rate difference   | $\ln(\Delta_{\lambda,i})$ | Normal(0,$\gamma_{\lambda,i}\sigma_\lambda\zeta$) |
| Per interval log-extinction rate difference   | $\ln(\Delta_{\mu,i})$ | Normal(0,$\gamma_{\mu,i}\sigma_\mu\zeta$) |
S8 Diversification rates with phylogenies

S8.1 Diversification shifts against simplified phylogenies

Figure S4: Speciation rates using the GMRF (red) and HSRMF (blue) models with daisy and grass (#1 and #2) phylogenies. Note that the most pronounced increase in speciation rates in both families occurred during the divergence of the largest clades and when all major subfamilies were already present. This indicates the global (i.e., tree-wide) impact of diversification rate change.
S8.2 Diversification shifts among lineages

Figure S5: Speciation (left), extinction (middle) and diversification (right) rates using the best fitting models (GMRF for daisies and HSRMF model for grasses (1)). For daisies, B: Barnadesioideae; M: Mutisioideae; C: Carduoideae; H: Helianthodae; S: Senecionodae; A: Asterodae; Ci: Cichorioideae. For grasses, P: Pooideae; B: Bambusoideae; O: Oryzoideae; P: Paniceae; Ch: Chlorioideae; Da: Danthonioideae; Ar: Aristidoideae. Note that the most pronounced increase in diversification rates occurred during the last ∼30 Mya in both families. Also note that diversification rates change while all subfamilies diversified. This shows the global (i.e., tree-wide) impact of the diversification rate change compared to a single or few clades driving the diversification rate changes.
The effect of different prior models on diversification rates

Figure S6: Diversification rate estimates using different prior models. The speciation, extinction and net-diversification rate estimates using the GMRF (red), HSMRF (blue) and UCLN (green) prior models. The rates were estimated using 100 epochs (for other numbers of epochs see Figure S7). The two autocorrelated models qualitatively agree on the estimated rates and infer diversification rate shifts driven by changes in the speciation rate. As expected, the GMRF model produces smoother rates while the HSMRF model produces more discrete jumps. The UCLN model produces strong variation which is a clear result of over-fitting (see Figure S8). Also note that this results cannot be due to non-identifiability of diversification rates because the episodic birth-death model used here is identifiable [13].
The effect of number of epochs on diversification rates

Figure S7: Diversification rate estimates for different number of epochs. We estimated diversification rates using $N = \{4, 10, 20, 50, 100, 200\}$ epochs for all three diversification prior models (GMRF, HSMRF and UCLN). The two autocorrelated models estimate smoother rate functions with higher number of intervals, as previously observed by Magee et al\[15\]. The uncorrelated model over-fitted when many intervals where used (see Figure S8).
### S11  Model selection of diversification models

| Model  | Marginal Likelihood | #intervals |
|--------|---------------------|------------|
| GMRF   | -23675              | 4          |
| HSMRF  | -23685              | 10         |
| UCLN   | -23680              | 20         |
|        |                     | 50         |
|        |                     | 100        |
|        |                     | 200        |

**Figure S8: Model selection between the three diversification rate prior models and for different number of epochs.** We estimated marginal likelihoods for all three diversification prior models (GMRF, HSMRF and UCLN) and for varying number of epochs, \( N = \{ 4, 10, 20, 50, 100, 200 \} \). The colored areas show (i) no significant support in white, (ii) support in light gray, (iii) strong support in gray, and (iv) decisive support in dark gray according to the common Bayes factor thresholds [12]. The UCLN model was always decisively rejected. The best fitting model for the daisy phylogeny was the GMRF with 200 epochs and the HSMRF with 100 epochs for the grasses phylogeny. Interestingly, only for \( N = 4 \) epochs was the UCLN model better (daisy dataset) or equally good (grasses dataset) but more epochs resulted in worse model fit (best fit for daisies was 10 epochs and 4 epochs for grasses).
The effect of different taxon sampling methods

Figure S9: Diversification rate estimates using different incomplete taxon sampling methods. We estimated the diversification rates using our newly developed empirical taxon sampling and the previously developed uniform taxon sampling. The diversification rates were estimates using a) the GMRF diversification rate prior model and b) the HSRMF diversification rate prior model. For each model with assumed $N = 200$ epochs. The estimated diversification rate differ depending on the incomplete taxon sampling method, but are similar between diversification rate prior models (see Figure S6). Thus, using the correct incomplete taxon sampling approach is crucial for unbiased estimation of diversification rates.
S13  The effect of different models on correlations to the environmental variable

![diagram](image)

**Figure S10: Estimating correlation between diversification rates and two environmental variables.** We estimated the correlation between atmospheric CO$_2$ and paleo-temperature (with environmental variables averaged in 1MY bins) to speciation and extinction rates using our four environmentally-dependent diversification models: fixed, UC, GMRF and HSMRF. The inset posterior probabilities show the posterior probability that the correlation factor $\beta$ is smaller than 0 (i.e., a negative correlation). If the posterior probability is close to one, then there is a significant negative correlation and if the posterior probability is close to zero, then there is a significant positive correlation. The speciation rate is negatively correlated with atmospheric CO$_2$ for the both the daisy and grasses datasets regardless of the chosen model. The extinction rate is also negatively correlated and shows the same trend as the speciation rate. The correlation between paleo-temperature and speciation rate is less certain: the fixed and UC model infer a negative correlation whereas the GMRF and HSMRF infer no correlation or a positive correlation. The HSMRF model was the best fit model for the paleo-temperature analyses (see Figure S11). The same trend is seen in both datasets for the daisies and grasses.
Model selection of environmental variable correlated models

Figure S11: Marginal likelihood estimates for the four environmentally-dependent diversification models. We estimated marginal likelihoods using stepping stone sampling for the four environmentally-dependent diversification models (\textit{fixed}, UC, GRMF and HSMRF) and two environmental variables (atmospheric CO$_2$ and paleo-temperature). Additionally, we binned the environmental variable in 1, 2.5 and 5 million year bins. We computed the marginal likelihoods for both the daisy and grasses dataset (calibration method #1). The shaded boxes represent significance levels according to standard Bayes factors\cite{12}: slightly support (white), supported (light gray), strongly supported (dark gray) and decisively supported (dark gray). We found that for the daisy dataset the best predictor is atmospheric CO$_2$ with 2.5 MY bins using the UC model. The binning size did not impact the results and the order of preferred models remained unchanged. For the grasses dataset, the \textit{fixed} model with atmospheric CO$_2$ as predictor variable in 2.5 MY bins received highest support. Interestingly, for the paleo-temperature as predictor variable the results flip with the two autocorrelated models (GMRF and HSMRF) receiving higher marginal likelihood than the \textit{fixed} and UC model. This is particularly important as for the atmospheric CO$_2$ all models agreed on the negative correlation between CO$_2$ and speciation rates, whereas for the paleo-temperature the results qualitatively differed from negative correlation (\textit{fixed} and UC) to no correlation or slightly positive correlation (GMRF and HSMRF); see Figure S10.
The effect of binning on environmental variable correlated models

Figure S12: Estimated correlation factor for different bin size of the environmental variable. We estimated the correlation factor $\beta$ between the speciation and extinction rates and the environmental variable (atmospheric CO$_2$ and palae-temperature) using the HSRMF model. The environmental variables were computed as averages for bins of size 1, 2.5 and 5 MY. The inset posterior probabilities show the posterior probability that the correlation factor $\beta$ is smaller than 0 (i.e., a negative correlation). If the posterior probability is close to one, then there is a significant negative correlation and if the posterior probability is close to zero, then there is a significant positive correlation. There is little effect on the correlation factor depending on the bin size, although a bin size of 5MY has the widest posterior distribution and is slightly shifted closer towards zero values and the posterior probabilities was less significant.
S16 The effect of node calibration on environmental variable correlated models

We compared the correlation factor between speciation and extinction rates and environmental variables (atmospheric CO\textsubscript{2} and paleo-temperature with averages over 1MY bins). The inset posterior probabilities show the posterior probability that the correlation factor $\beta$ is smaller than 0 (i.e., a negative correlation). If the posterior probability is close to one, then there is a significant negative correlation and if the posterior probability is close to zero, then there is a significant positive correlation. We applied the HSRMF model to the two grasses phylogenies obtained under different calibration scenarios (scenario #1 younger and scenario #2 older). For scenario #1 we estimate a negative correlation between atmospheric CO\textsubscript{2} and speciation rates but not correlation to paleo-temperature. For scenario #2 we estimate a positive correlation between speciation rates and paleo-temperature but no correlation to atmospheric CO\textsubscript{2}.

Figure S13: Estimated correlation factor $\beta$ for the grasses dataset depending on node calibration scenario.
The effect of environmentally-dependent diversification models on diversification rates

Figure S14: Estimated diversification rates for the daisy phylogeny. Here we compare the estimated diversification rates of our environmentally-dependent models to the null-hypothesis without environmental dependence. The environmentally dependent HSMRF and GMRF models yield extremely similar diversification rates compared with the environmentally independent diversification rate estimates. This shows that the diversification rates are not forced due the environmental correlation, but instead are driven by the information in the data (the phylogeny with divergence times). The uncorrelated (UC) rate models shows very different diversification rates for the correlation with paleo-temperature which confirms the disagreement in correlation factors (Figure S10). Unsurprisingly, the fixed environmentally-dependent diversification rate model show diversification rate closely following the environmental variable because no other source of rate-variation is allowed. Thus, all diversification rate variation in the fixed model, e.g., when using paleo-temperature as the environmental variable, is misleading because it is wrongfully enforced by the environmental variable.
Figure S15: Estimated diversification rates for the grasses phylogeny (calibration scenario 1). Here we compare the estimated diversification rates of our environmentally-dependent models to the null-hypothesis without environmental dependence. For the CO₂ as the environmental driver, we see that all four environmentally-dependent diversification models provide very similar diversification rates. This confirms the agree that all models infer a correlation between CO₂ and diversification rates in grasses (Figure S10). Conversely, the diversification rates of all four models disagree if paleo-temperature is used. Thus, the correlation between paleo-temperature and diversification rates is unreliable and dependent on the specific model.
S18 Simulation study of environmentally-dependent diversification rates

S18.1 Simulated diversification rates under environmentally-dependent diversification rates models

Figure S16: Speciation rates simulated under an environmentally-dependent GRMF diversification model. We simulated speciation rates with different correlation factors $\beta = \{0, -0.005, -0.01\}$ and standard deviations $\sigma = \{0, 0.02, 0.04\}$. We used the atmospheric CO$_2$ as the environmental variable. When $\beta = 0$ in the simulations, then this model was equivalent to an environmentally-independent diversification model. When $\sigma = 0$ in the simulations, then this model was equal to the fixed environmentally-diversification model. When both $\beta = 0$ and $\sigma = 0$, then we simulated under a constant rate process (top left). This establishes the false positive rate in our simulations. Note that the autocorrelated model (GMRF) has overall more variation in speciation rates (e.g., top right) compared to the uncorrelated model (Figure S17) because the variation is additive over epochs in the autocorrelated model.
Figure S17: Speciation rates simulated under an environmentally-dependent UC diversification model. We simulated speciation rates with different correlation factors $\beta = \{0, -0.005, -0.01\}$ and standard deviations $\sigma = \{0, 0.02, 0.04\}$. We used the atmospheric CO$_2$ as the environmental variable. When $\beta = 0$ in the simulations, then this model was equivalent to an environmentally-independent diversification model. When $\sigma = 0$ in the simulations, then this model was equal to the fixed environmentally-diversification model. When both $\beta = 0$ and $\sigma = 0$, then we simulated under a constant rate process (top left). This establishes the false positive rate in our simulations. Note that the autocorrelated model (GMRF, Figure S16) has overall more variation in speciation rates (e.g., top right) compared to the uncorrelated model because the variation is additive over epochs in the autocorrelated model.
S18.2 Simulated phylogenies under environmentally-dependent diversification rates

Figure S18: Lineage-through-time (LTT) curves of 10 phylogenies simulated under an environmentally-dependent GRMF diversification model. We used the simulated diversification rate trajectories shown and described in Figure S16. We nicely observe the log-linear LTT curve for the constant-rate birth-death simulations (top left) and increasing deviation from the log-linear curve with higher correlation factor $\beta$. Higher standard deviation $\sigma$ in the speciation rates led to slightly more variation in LTT curves but no large effect.
Figure S19: Lineage-through-time (LTT) curves of 10 phylogenies simulated under an environmentally-dependent UC diversification model. We used the simulated diversification rate trajectories shown and described in Figure S17. We nicely observe the log-linear LTT curve for the constant-rate birth-death simulations (top left) and increasing deviation from the log-linear curve with higher correlation factor $\beta$. Higher standard deviation $\sigma$ in the speciation rates led to slightly more variation in LTT curves but no large effect.
S18.3 Estimated correlation factors from the phylogenies simulated under environmentally-dependent diversification rates

Figure S20: Estimated correlation factors for the simulated phylogenies under the GMRF environmentally-dependent diversification rates model. We estimated correlation factor $\beta$ using the simulated phylogenies shown and described in Figure S18. We used all four environmentally-dependent diversification rates model for inference, running in total 450 MCMC analyses. Overall, all four models perform well to estimate the environmental correlation. As we noticed in our simulations, the diversification rate variation is primarily driven by the environmental variable and less by additional factors (comparably low $\sigma$). In these situations it does not matter much which environmentally-dependent diversification rates model is used. Nevertheless, the HSRMF model always produced the smallest credible intervals and was most precise. This simulation study shows that there is high power to detect environmental correlation to diversification rates (middle and bottom row) while retaining a low false-positive rate (top row). The results are congruent with our inferences using the simulated trees under the UC environmentally-dependent diversification rates model (Figure ??).
Figure S21: Estimated correlation factors for the simulated phylogenies under the UC environmentally-dependent diversification rates model. We estimated correlation factor $\beta$ using the simulated phylogenies shown and described in Figure S19. We used all four environmentally-dependent diversification rates model for inference, running in total 450 MCMC analyses. Overall, all four models perform well to estimate the environmental correlation. As we noticed in our simulations, the diversification rate variation is primarily driven by the environmental variable and less by additional factors (comparably low $\sigma$). In these situations it does not matter much which environmentally-dependent diversification rates model is used. Nevertheless, the HSRMF model always produced the smallest credible intervals and was most precise. This simulation study shows that there is high power to detect environmental correlation to diversification rates (middle and bottom row) while retaining a low false-positive rate (top row). The results are congruent with our inferences using the simulated trees under the GMRF environmentally-dependent diversification rates model (Figure S21).
Figure S22: Lineage-through-time curves of simulated phylogenies under empirical sampling. We simulated 100 phylogenies (only first 10 shown here) under a constant-rate birth-death process (false-positive) and an episodic-birth-death process (power) using empirical taxon sampling. These trees were simulated by adding the missing species randomly in the pre-assigned clades of the daisy phylogeny. Then, we simulated divergence times under either the constant or episodic birth-death process. After simulation, the additional taxa were pruned again to mimic empirical sampling. The solid black line shows the empirical LTT curve of the daisy phylogeny.
Figure S23: Estimated net-diversification rates using the simulated phylogenies from Figure S22. The solid black line shows our true net-diversification rates. If our assumption of incomplete taxon sampling matches the simulation conditions, then we infer unbiased diversification rates, as previously shown under similar incomplete taxon sampling schemes [11, 10, 18]. Conversely, if the incomplete taxon sampling assumption is violated, e.g., assuming all missing species are uniformly distributed within the phylogeny, then we obtain strongly biased diversification rates. We also note that our GMRF model shows a good performance even when the true diversification rates are constant (top left, low false-positive rate). Our good precision in not surprising because the simulated phylogenies had 2723 tips, as our daisy phylogeny.
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