Design of a Didactical Activity for the Analysis of Uncertainties in Thermography through the Use of Robust Statistics as Teacher-Oriented Approach

Pablo Rodríguez-Gonzálvez 1,* and Manuel Rodríguez-Martín 2

1 Department of Mining Technology, Topography and Structures, Universidad de León, 24401 León, Spain
2 Department of Mechanical Engineering, Universidad de Salamanca, 49029 Zamora, Spain; ingmanuel@usal.es
* Correspondence: p.rodriguez@unileon.es; Tel.: +34-920-44-2055

Abstract: The thermography as a methodology to quantitative data acquisition is not usually addressed in the degrees of university programs. The present manuscript proposes a novel approach for the acquisition of advanced competences in engineering courses associated with the use of thermographic images via free/open-source software solutions. This strategy is established from a research based on the statistical and three-dimensional visualization techniques over thermographic imagery to improve the interpretation and comprehension of the different sources of error affecting the measurements and, thereby, the conclusions and analysis arising from them. The novelty is focused on the detection of non-normalities in thermographic images, which is illustrates in the experimental section. Additionally, the specific workflow for the generation of learning material related with this aim is raised for asynchronous and e-learning programs. These virtual materials can be easily deployed in an institutional learning management system, allowing the students to work with the models by means of free/open-source solutions easily. Subsequently, the present approach will give new tools to improve the application of professional techniques, will improve the students’ critical sense to know how to interpret the uncertainties in thermography using a single thermographic image, therefore they will be better prepared to face future challenges with more critical thinking.

Keywords: thermography; engineering; education and training; innovation; 3D imaging; virtual laboratory; e-learning

1. Introduction

Thermography allows the measurement of an object’s temperature remotely in a non-invasive way, being its main added value the fact that provides an image instead of a single measurement [1,2]. The thermographic camera allows to record the infrared radiation (IR) emitted by bodies as images, and since the emitted radiation is related to the superficial body’s temperature, the IR camera allows the calculation and visualization of the superficial temperature by means of the thermographic images (also called thermograms).

Due to the non-invasive nature of thermography, this has been positioned as a pivotal technique in engineering due to its multiple applications in a large variety of fields [3–6]. Not only that, but under the paradigm of the Industry 4.0 revolution, companies are requiring professionals able to apply new procedures to obtain the required flexibility and interoperability [7]. Therefore, multidisciplinary teaching will improve students’ abilities to face the future challenges [8]. Thermography is also of interest in predictive maintenance tasks due to the fast transformation of Industry 4.0 [9]. Moreover, it is susceptible to be combined with machine/deep learning approaches to achieve profitable predictive maintenance as in [10] where is presented a fuzzy system-based thermography approach for predictive maintenance on electric railways and, also, predictive methods for defect detection in materials [11].
The use of IR cameras in academic institutions is limited due to their economic cost, which is usually high, and therefore difficult to acquire high-end models due to the budget constraints. However, to specific applications, the low-cost alternatives could be applied [12]. Examples of the use of IR cameras in the academic context include the visualization of the superficial distribution of engine temperatures [13], the acquisition of accurate real-time measurements for the analysis and calculation of the different configurations of collectors [14], as well as a wide range of physics and chemistry experiments, as for example the thermal conductivity and the heat transmission by conduction, energy transformations, the dissipation of mechanical energy and other [15,16] and the detection and evaluation of thermal bridges [17]. Thermography has been also applied has in the training of professionals not directly related to engineering and experimental sciences, for example, for the training of primary teachers in the context of ecocentric education [18,19].

Furthermore, the progressive conversion from traditional educational programs to online/asynchronous ones has placed the virtual laboratory paradigm in a pivotal place in engineering programs [20,21], especially the development lines related to low-cost implementation and sharing use of resources [22]. These conversion processes have taken on greater importance in the current context of the pandemic, in which many university programs have switched to e-learning and b-learning.

In this regard, the novel use of 3D visualization software in learning [23] benefits the students in the acquisition of skills and competences, especially the transversal ones. Please note that this type of software was initially used for tasks related to Geomatics, but the large number of sensors and the development of applications oriented to the three-dimensional reconstruction have increased industrial interest.

In addition to the visualization, students can asynchronously interact with the virtualized learning materials (for example, taking measurements, establishing regions of interest (ROI’s), extracting sections, etc.) thanks to the wide choice of free/open-source visualization software currently available in combination with the remote tutoring of the professor and the support given using Learning Management Systems (LMS) in b-learning and/or e-learning environments.

1.1. Professional Challenges

The acquired competences, abilities, and skills represent the personal qualification to fulfil certain functions in a competent way, related to professional occupation. So, the learning processes should be focused to train the student to become a competent professional. Despite this, not all industrial and productive environment factors can be simulated in the courses, so the practical tasks should be as close as possible to the industrial environment. Furthermore, the professors should assure that the future workers will be prepared to face the Fourth Industrial Revolution, to articulate the knowledge and to learn new technical skills to overcome situations never faced at the training courses [24].

The present manuscript is focused on a specific issue of this new context, which is the usage of thermographic camera for civil and industrial tasks, which encompass from the detection of anomalies and to the development of simulation models related to obtaining thermal properties such as the emissivity and the heat transfer coefficient, based on thermal gradients, heat distributions, isotherms, and cooling/heating speed. However, more classic applications, such as the use of infrared thermography (IRT) as a visual inspection tool (qualitatively), which is usually employed in the electric systems, predictive maintenance, thermal bridges detection, and other uses. Please note that infrared thermography applied to buildings is not always applied using the passive modality, since in many situations a thermal stimulation of the materials is required; in some cases, the sun is exploited for heating a façade. However, the present teaching-learning activity is based on the passive one, which is the typical one to observe the entire building structure [25].

The standards developed for the application of infrared thermography in buildings address different issues related to thermal inspection, like BS EN 13187:1999 [26] which specifies a qualitative method, by thermographic examination, for detecting thermal irreg-
ularities in building envelopes; EN ISO 6781-3:2015 [27] which specifies the qualifications and competence requirements for personnel who perform thermographic investigations on buildings, interpreter the data and report the results; ISO 14683:2017 [28] which deals with simplified methods for determining heat flows through linear thermal bridges which occur at junctions of building elements, or ASTM E1311 [29] which refers to the standardized test method for minimum detectable temperature difference for thermal imaging systems. Moreover, it is possible to find in the scientific literature studies related to the application and/or research of thermographic process for building diagnostics. Due to the extent of it, we refer the reader to the next selected articles: A review of the active IR thermography for detection and characterization of defects in reinforced concrete [30], and a general review of both approaches active/passive [31,32].

Some of the main uses of IR images in passive modality are related to the maintenance and inspection tasks. For these, thermography is used to diagnose the buildings/systems, and to schedule the repairs, predict and/or report failures, and/or document its lifecycle. Since the engineers responsible for maintenance works have to base their decisions on the thermographic images, several uncertainties could arise during the image acquisition phase, and therefore they will influence the final decision-making. This need is even more critical when the images are really captured by a maintenance operator without specific knowledge of thermography and infrared radiation, since her/his skill will be another source of uncertainty, as the working environments o the technical specification of the IR camera (also considering the physical difficulty of accessing and inspecting certain machines and devices in complex industrial feasibilities).

By the proposed approach, future engineers could assess the level of uncertainty of the maintenance and inspection tasks, which are related to buildings/systems and other physical parameters as the emissivity since the temperature values obtained using thermography are strongly dependent on the emissivity value of the material [33], but also other such as humidity, undesired thermal reflections, etc. Thus, this prior small uncertainty could be propagated to the global system, and the combined uncertainty could be increased, causing problems for the interpretation and validation of thermographic images.

1.2. Classical Teaching Approach

On the classical teaching approach, the relevance of a proper set of the parameters related to temperature (measurement by IR cameras), is exemplified by exercises that follow a structure as follows:

"To determine the superficial temperature of an object, it is considered an emissivity of \( \varepsilon_1 = 0.1 \). As a result, the final temperature is \( T_1 = 150 \) degC. If the emissivity is really \( \varepsilon_2 = 0.2 \), determine the temperature \( T_2 \) and quantify the error."

Students are taught to use the Stefan-Boltzmann law (1) to relate the temperature change to the fourth power of the emissivity ratio.

\[
T_2 = T_1 \cdot \left( \frac{\varepsilon_1}{\varepsilon_2} \right)^{\frac{1}{4}}
\]  

Therefore, for this example \( T_2 \) is equal to 83 degC, being the error committed 67 degC. These kinds of basic examples are very useful for learning about phenomena related to radiation but does not provide insights about the use of IR images in real conditions, and therefore the students’ skills will not be completely developed. This article proposes a new teaching methodology in which the student can discover the limitations of the thermographic technique. This way, in the future, students will be able to know and control all the parameters involved and develop their critical sense to avoid errors derived from an inadequate interpretation of the thermographic image.

Regarding the teaching of thermographic image processing methods, the camera manufacturer’s own software is usually used, which allows changing the colour palette, evaluating trends, working with regions of interest, etc. However, these methods do not
specify if the statistics used are useful to evaluate in-depth the temperature and/or infrared radiation variations. Therefore, it is necessary a study of the statistical distributions in thermography so that the student can be critical of the results obtained and the way to interpret them.

1.3. Research Question

For all of the above, the next research question guided the present article: This research aims to evaluate the possible uncertainties in thermographic images. In this way, it will be possible to instruct the students in robust methods that allow obtaining quantitative and qualitative information without committing errors in the interpretation of results.

Therefore, the novelty of the present work is focused on a thermographic approach in the context of education carried out through the application of a workflow based on specific tasks for three-dimensional point clouds processing which have been researched and successfully applied in engineering programs for other issues [23]. Please note that this approach is not the one usually used in thermography teaching and allows the students to be much more critical with the data to achieve a proper interpretation.

The remainder of the article is structured as follows. In Section 2 is presented the thermal imaging fundamentals, whereas the design of the learning activity is shown in Section 3. The output of the activity is presented in Section 4 in both qualitative and quantitative terms. Lastly, Section 5 discusses the main conclusions.

2. Theoretical Background

The primary use of IR imaging is the 2D matrixial representation of the temperature distribution of an object’s surface and/or scenario. Despite its usefulness in numerous disciplines, the usage of IR imaging is often reduced to the mere display of the IR image in a qualitative way using a personalized color palette, rather than using the temperature values recorded in the image. Although the use of a color ramp (or color palette) by means of a lookup table enhances the understanding of the underlying information contained in the thermogram, the comparability of the different images is limited by the definition of the lookup table, namely, if the scale is linear or logarithmic, if it is a conventional palette shared by different software or one customized by the user or specifically used by a particular program. Thus, the analysis could be biased, and consequently, the conclusions drawn from the use of the same set of thermal images could differ according to the approach used.

In this regard, it is not uncommon to find even analysis based on the digital levels of the color palette in the professional practice. In this regard, students may confuse the “part” with the “whole”. In other words, students may be satisfied with the color information provided by the camera without having critical thinking about what that palette represents, its limitations, and the bias of the capture process.

Consequently, this subsection is dedicated to defining the relationship between the radiance values (collected by the IR camera) and the resulting temperature values, in order to identify the variables that might affect the outcome of the thermographic inspection and bias the subsequent decision-making process. However before that, we need to mention the different IR thermal imaging techniques to put in context the significance of those variables. In this manner, thermal imaging can be categorized as follows [34]:

1. **Qualitative**: Relative changes are monitored through regular observation and registration of IR imaging without a numerical dataset as support.
2. **Quantitative**: Superficial distribution or punctual temperature values are expressed in absolute terms. Therefore, even minor variations caused by the modification of the variables used for temperature calculation and field data acquisition (e.g., emissivity, atmospheric parameters, etc.) may lead to measurement inaccuracies in the absolute values calculated [35].

Because of the awareness of possible measurement errors in quantitative thermography, it is recommended to use external reference temperature sources, especially with modern cameras based on uncooled detectors [36]. It is often necessary to use mixed
approaches that require both qualitative inspection and qualitative measurement of certain thermal parameters.

The principal parameters that influence the calculation of temperature for passive thermographic inspection are:

- Object emissivity.
- Relative humidity of the atmosphere.
- Projected solid angle. Please note that it, jointly with the detector area (which is a fixed value), can be expressed as a function of the object distance.
- Reflected ambient temperature, or the temperature of the object surroundings.
- Atmospheric temperature.
- Undesired infrared reflections and shadows in the monitored object can also affect the accuracy of the measurement; however, the effect cannot be quantitatively corrected in an easy and standard way. The camera operator should empirically try to identify such sources and try to vary the perspective to study possible variations in the temperature distribution.
- Camera calibration, since there could be calibration shifts due to electronic component aging.

By far, the emissivity is the main feature of the object’s surface, since it has an impact on the amount of energy that it is emitted under stationary thermal conditions \[37\]. In the case of the analyzed surface has the properties of a blackbody (BB), it is possible to determine the radiant exitance by means of Planck’s law \(2\) for a specific wavelength \(\lambda\) and fixed temperature \(T\):

\[
T_{BB}^{\lambda} \text{(degC)} = \frac{c_2}{\lambda \ln \left( \frac{c_1 \lambda^3}{W_{bb}} + 1 \right)} - 273.15
\]

where \(c_1 = 2 \cdot \pi \cdot h \cdot c^2\)

\[
c_2 = \frac{k}{\lambda}
\]

and

where \(c_1\) and \(c_2\) are constants in function of the Planck’s constant \(h\), the Boltzmann’s constant \(k\), and the velocity of light \(c\); whereas \(W_{bb}\) is the spectral radiant emittance from a blackbody with \(T\) temperature at wavelength \(\lambda\). Please note that the spectral density cannot be measured for one exact wavelength, since the energy transfer is zero for a single wavelength, it is always measured for a certain wavelength range within the electromagnetic spectrum, which is usually from 8 to 14 microns. Nonetheless, given that real bodies emit only a fraction of the thermal energy \(W_{o}\) emitted by a blackbody at the same temperature \(W_{bb}\), the final temperature values will be modified. This relationship is related to the emissivity \(\varepsilon\) as stated in the following Equation \(3\):

\[
\varepsilon_{\lambda} = \frac{W_{Ao}}{W_{bb}}
\]

Of all the parameters, emissivity is perhaps one of the most critical \[33\] and the most difficult to estimate because it depends on many properties of the object, such as the material, the homogeneity of the object’s surface or the surface finish, the state of deterioration, etc. Despite its relevance in the calculation of temperature, emissivity is a parameter that is often determined with low precision. As a result, the error related to emissivity propagates to the computed superficial temperature of the object, especially when working with absolute temperature values of different objects. In the case of elements with a surface finish with high emissivity values, they will have associated a low reflectance, and therefore, the superficial temperature will be measured easier with the IR camera.

Many non-metallic materials show a high emissivity with a relatively constant trend regardless of their surface characteristics, at least in long-wave spectral ranges (see Table 1). Countless materials have been differentiated, and their emissivity values are listed in tables like the following:
Table 1. Emissivity values of various common materials over the range of 8–14 microns. Adapted from [38].

| Material                  | Emissivity       |
|---------------------------|------------------|
| Asphaltic concrete        | 0.94–0.97        |
| Brick                     | 0.93–0.94        |
| Wood                      | 0.93–0.94        |
| Portland cement concrete  | 0.92–0.94        |
| Paint                     | 0.90–0.96        |
| Granitic rock             | 0.83–0.87        |
| Glass                     | 0.77–0.81        |
| Sheet iron (rusted)       | 0.63–0.70        |
| Polished metals           | 0.16–0.21        |

Please note that the values of Table 1 are related to a specific ambient temperature, and any temperature change will lead to emissivity changes. They are also based on standard surface conditions. When the surface quality or coating of the material changes, the emissivity value can be different.

The remaining four parameters are linked to the environment and the atmospheric conditions and characterize the atmospheric transmittance. As these variables are measurable up to with certain precision, they will influence temperature calculation (2).

The five aforementioned parameters are the key ones to compute the temperature, but, in a broad vision and according to [39], they can be complemented with the camera positioning, and in active thermography, also by the intensity, frequency, and the rest of characteristics of the stimulation sources.

The positioning error is of interest when multiple measurements of the same region of interest are carried out. Since this can be minimized by the use of a tripod or another camera fixing system, and the possible position variation for every capture or measurement, this could be dismissed due to the final pixel size (related to the object-sensor distance), this error source will be neglected in the next sections.

Another intrinsic error source that could be taken into account is the one related to the preheating time of the IR camera. The cameras should work at an optimal working temperature, so the acquisition of images without this heating time could generate an error in image series. Since this error source is linked to the proper handle of the camera, it can be considered a gross error, therefore it will be not studied in the following sections.

In the following section, the design of the activity will be described, so that the student can simulate and evaluate the results with a double approach (quantitative and qualitative) under different conditions. Consequently, the student will be able to raise questions, like:

Which would be the most critical atmospheric variable for the study case? or What is the admissible relative error accordingly to the purpose of the thermal inspection?

And derive helpful insights for his/her learning process.

3. Methodology

As stated in the introduction, the focus of the article is the design of a learning activity that will allow the students to understand the uncertainty sources derived from the temperature measurement by means of IR images. The activity is based on the inspection of building facades, since this is important for the training of engineers and one of the most widespread applications of thermography both for inspection and documentation tasks and for energy efficiency tasks. Furthermore, this activity is easy to interpret, with intuitive results, and multidisciplinary useful for various engineers of different specialties. However, firstly, it is necessary to state briefly the typology and characteristics of those measurement errors, which can be random or systematic.

The International Vocabulary of Metrology (VIM) [40], defines the systematic measurement error as the part of the measurement error that remains constant or varies predictably...
in replicated measurements, whereas random or Gaussian measurement error is the constituent of the measurement error that varies unpredictably in replicated measurements. Thus, the correction of systematic error sources improves the measurement accuracy, defined as the closeness of agreement among measured quantity values obtained by replicated measurements on the same or similar objects under specified conditions [40].

The digital levels (DL) obtained from the IR images can be used only for visualization purposes, but not for quantitative thermography, as they are affected by the application of the specific lookup table (color palette) and/or the modification applied over the histogram.

The software supplied by the manufacturer usually allows the measurement of individual temperature values for each pixel. However, such values are influenced by the field parameters of data collection, so they must be adjusted through an adequate analysis and critical reflection made by the students. In other words, the temperature measurement for each point (that is easily extracted from the pixel value of the IR image using manufacturing software) may not be reliable and students should know it.

To facilitate the handling of these error sources, the recorded raw radiance values have to be retrieved from the IR images and stored in an open file format. Thus, it can be manipulated and/or visualized with any scientific software package used in engineering degrees. The IR images, despite being stored in an image compressed format (.jpg), incorporate all the recorded raw radiance values and also the camera metadata needed to calculate the superficial temperatures [41].

The workflow related to the generation of 3D thermographs and their visualization is shown in Figure 1:

**Figure 1.** Workflow for the generation and visualization of 3D thermographs.

A specific workflow is used to display the results, which converts the thermograms into 3D viewable models, but with a unique feature: the third axis does not actually represent the elevation, depth, or any metric value, but the temperature of the object surface [41]. This method has been used with success in the subjects of health sciences degrees for blood flow monitoring and also for emotions [42].

In the initial phase (Figure 1), the radiance measurement is extracted (raw) from the images acquired in the field. Thus, the students can manage the calculation of the temperature and modify the error variables. This operation will be supervised by the professor according to the competences to be acquired. The extraction of the raw radiance data can be done with the Exiftool [43], which is an open-source meta-information reader/writer. This application allows the users to read and modify the EXIF metadata tags of image files, including IR images. By means of a personalized query, it is possible to obtain both the raw digital levels in a 16-bit format and the sensor’s metadata. The latter is highly relevant, and it should be taking into account since it contains the custom sensor’s coefficients necessary for the conversion of the DL to radiance values. Please note that these coefficients are specific for each thermal camera.
After obtaining the recorded radiance values, the calculation of the surface temperature is quite simple through a script on the scientific calculation package. The authors recommend the use of GNU Octave [44], which is open-source, but more alternatives are available depending on the functionalities supplied as well as the requirement of the teaching, such as Scilab [45], or Freemat [46]. At this point, the student or the professor can alter the five input parameters to show the effect on the computation of the final surface temperature, not only numerically but also in terms of its distribution. In addition, it is possible to apply a threshold over the IR image to isolate the significant temperature interval.

The output thermogram remains a 2D image, so it shares the same limitations or interpretation as conventional approaches, for example, the use of unintuitive software to query the surface temperature values of each individual pixel; limited spatial analysis functionalities; or the visualization constrained by the available color palettes. To avoid, or at least minimize, these constraints, the authors propose the use of visualization software from Geomatics engineering. In addition, its suitability in teaching is supported by the argument that the visualization software to be employed by the students has to be open-source (or at least free or free under student license), in order to facilitate its implementation in the teaching strategies and that the student can have the software available anywhere and on any computer. The recommended option is CloudCompare [47], but as in the preceding case, there are also other free alternatives available, such as Meshlab [48]. CloudCompare allows 3D editing operations, like measurement, model segmentation and/or sectioning, slicing, adjustment based on parametric surfaces, etc. All these operations can be carried out by the students easily. Moreover, this software offers the professor tools to enhance the visualization of the models such as smooth filters, or the creation of meshes. The goal of the visualization strategy is to facilitate the students the analysis of the thermograph as a 2D entity (like a conventional image) but also as a 3D entity that represents the surface temperature along the third axis.

The activity design was carried out following the three criteria for the creation of virtual models in the context of the virtual environment and virtualization of materials established in previous works [21,49], and summarized as quality, economy, and reality criterion. Please note that geometrical precision is not a fundamental parameter to be optimized for this task. However, when performing the thermographic capture is necessary to avoid aberrations or distortions that compromise the geometric fidelity of the objects that appear in the image.

Although these criteria were originally established for the creation of virtual laboratories, given the inherent nature of the current activity, they can be used as guidance for its design and to evaluate the students’ competences [50]. Therefore, they have been adjusted for the learning objective of the activity (Table 2):

| Table 2. Criteria for the methodological design. |
|--------------------------------------------|
| **Criterion** | **Description** |
| Reality | Illustrate how slight changes in particular variables alter the superficial temperature values |
| | Offer the option of designing an evaluation on the virtual models |
| | Working on real images in a real context such as building inspection |
| Economic | Flexibility to repurpose the virtual learning material for subjects of other engineering courses |
| | Integration into the institutional LMS |
| | Visualization through free/open-source software |
| | Low computational weight |
| Quality | Results within acceptable limits for learning purposes |
| | Evaluation of competences |
| | Possibility of adding presentations, documents and/or other content-related files to the work package |
| | Geometrical precision |
The teaching workflow is structured following the work [50], and it includes the following steps: Presentation of the activity to the students, theoretical lesson about thermography and aims of the activity; training to use the 3D geomatic visualization software; autonomous and asynchronous work of the students; and finally, the activity submission on the LMS platform. This workflow is summarized in the next figure (Figure 2):

![Figure 2. Workflow for the activity designed.](image)

4. Results

The outcomes of diverse data acquisition configurations can be evaluated by the students in a dual approach: visually (qualitative analysis) and numerically (quantitative analysis). Consequently, students will obtain a more complete vision of the underlying problem of computing temperature from an IR camera (FLIR E6). This thermographic camera was chosen because it is mid-low range, useful for maintenance and evaluation of constructions tasks, and with similar characteristics to the cameras that students could use in their future work.

The camera’s thermal sensitivity is 0.06 degC, whereas the expected accuracy of temperature measurement is ±2 degC or ±2% of reading. Its sensor is a Focal Plane Array, uncooled microbolometer, with a spatial resolution of 5.2 mrad (160 × 120 pixels), capturing radiation between a wavelength of 7.5 μm and 13 μm.

4.1. Qualitative Results

The easiest and most direct approach to interpreting the outcomes is a 3D thermogram as shown in the next figure (Figure 3). In this figure it is compared the input IR image with the 3D visualization with a customized color palette. The color palette of the 3D view can be adjusted very easily by the students and does not modify or constraint the query of the superficial temperature.

![Figure 3. Comparison of the (a) acquired IR image; and (b) the converted 3D thermogram in flat view.](image)
Figure 4a shows the 3D view of the 3D thermogram, whose relief is not the topographical surface of the building but the façade’s surface temperature. Consequently, the student can identify more easily the different areas of contrast and heat exchange. In Figure 4b the temperature of the same façade is emphasized to highlight the measurement noise as well as the contrast areas. As the reader can appreciate, the first takes a granulated appearance.

\[ \text{Figure 4. 3D thermogram: (a) 3D view; (b) and detail of the temperature values of the façade on a magnified temperature scale.} \]

Among the tools provided by CloudCompare, it is worth mentioning the Eye-Dome Lighting real-time shader [51]. Although this plug-in aims to enhance the display of large-scale unorganized point clouds without the need for additional pre-calculation, it can be used to emphasize edges and surface relief (Figure 5). The third axis, defined orthogonal to the image plane, represents the temperature, and thanks to the aforementioned tool, allow to observe significant local changes in temperature even without the application of a color palette. Furthermore, CloudCompare allows applying a subsampling process in order to remove points in a homogeneous way to generate files with less computational weight, more suitable for the LMS.

\[ \text{Figure 5. Enhanced visualization by a real-time shader on the 3D thermogram without a color palette (only geometry).} \]

The 3D model allows the students to consult interactively the temperature and the position of any point. Given that this 3D thermogram is produced in the absence of any additional data (for example; a range-sensor and/or 3D model of the object/scenario) there is no additional metric information other than the pixel coordinates of the point. These can be transformed into metric units by knowing precisely the distance between the sensor and the façade, but under the hypothesis that the sensor plane is parallel to the façade. The precise scaling of the 3D thermogram is not a priority task for the teaching-learning process, since the present approach can be adapted to multiple kinds of objects and scenarios of the engineering subjects. Among the different tools provided by the visualization, is the option
to thresholding the surface temperature values to segment the façade and emphasize the critical areas. Such segmentation is done in a three-dimensional space, so students will also improve the competences related to spatial vision.

4.2. Quantitative Results

The conventional numerical analysis of thermographic images can be 1D as the simple consultation of individual pixel digital values, or 2D analysis like cross-sectional and longitudinal profiles. However, a 3D point cloud has been generated as a novel virtual material from the original IR image, being possible to extend the analysis to illustrate how altering one or more data acquisition variables (object emissivity, atmospheric parameters, object distance, etc.) impacts the computation of temperature, not only numerically, but also spatially. This analysis can be done for the whole study area or to a detailed area to raise the students’ awareness about a determined phenomenon [52]. In the next figure (Figure 6) is shown the 3D thermogram of a building façade computed using the correct field values of the aforementioned five parameters (Figure 6a) and with less accurate ones. The field data acquisition parameters are shown in Table 3. The computation was carried out according to the pipeline described in Section 3.

![Figure 6. 3D thermograph computed with: (a) correct field data acquisition variables; and (b) incorrect field variable.](image)

Table 3. Parameters of field data acquisition (capture values) and tested values to illustrate the thermographic discrepancies.

| Parameter       | Capture Value | Tested Value |
|-----------------|---------------|--------------|
| Ambient Temp.   | 21 degC       | 16 degC      |
| Humidity        | 57%           | 42%          |
| Distance        | 25 m          | 20 m         |
| Emissivity      | 0.95          | 0.90         |
| Reflected Temp. | 21 degC       | 16 degC      |

Likewise, it is possible to carry out the operation of map algebra (typical of Geomatics engineering), to subtract the temperature values from the modified 3D thermogram with respect to the one with the correct field data acquisition parameters. This technique is performed with a Geomatic software as CloudCompare [47]. In Figure 7a it can be easily seen that the temperature discrepancies are not homogeneous, and they are interrelated with the materials and shape of the façade [52]. The quantitative overview of the spatial distribution of the temperature differences is depicted as a histogram (Figure 7b).
Figure 7. Analysis of thermographic discrepancies: (a) discrepancies in superficial temperature by the variables’ errors; (b) histogram of the discrepancies.

Complementarily it can be studied the individual contribution of different error sources considered. In Figure 8 it is shown the 3D thermograph for the different data acquisition parameters (Table 3).

Figure 8. Modification of field acquisition parameters: (a) Ambient temperature; (b) Humidity; (c) Distance; (d) Emissivity; (e) Reflected temperature. Please note that the color palettes are different for each sub-image.

As surface temperature discrepancies are influenced by the specific emissivity values of each patch, their area, and spatial position, the errors will not be random, hence the hypothesis of Gaussian distribution will not be fulfilled. Thus, the customary Gaussian statistical parameters, as the mean and standard deviation, will not represent correctly the multiple error sources and their effect on the final IR image, that is why their use to assess the dispersion and central tendency of the data may not be appropriate. This problem is shown in Figure 9 both in the histogram and the overlapped Gaussian distribution curve; the Quantile-Quantile (Q-Q) plot; and the Percentile-Percentile (P-P) plot [53].
Because non-compliance with the assumption of normality will influence the analysis and bias the derived conclusions [54], a robust statistical approach is presented as part of the activity. In this case, the following robust estimators are adopted in the present study: the median—$m$, the normalized median absolute deviation—NMAD (4), the square root of the biweight midvariance—BwMv (5), and the interpercentile ranges (IPR).

NMAD = $1.4826 \cdot \text{MAD}$

BwMv = \[
\frac{n \cdot \sum_{i=1}^{n} a_i (x_i - m)^2 (1 - U_i^2)^4}{(\sum_{i=1}^{n} a_i (1 - U_i^2) (1 - 5 \cdot U_i^2))^2}
\]

\[
a_i = \begin{cases} 
1, & \text{if } |U_i| < 1 \\
0, & \text{if } |U_i| \geq 1 
\end{cases}
\]

\[
U = \frac{x_i - m}{9\text{MAD}}
\]

Being the median absolute deviation—MAD (8), i.e., the median ($m$) of the absolute deviations from the data’s median ($m_x$):

\[
\text{MAD} = m(|x_i - m_x|)
\]

Therefore, the median is used as a robust measure of the central tendency of thermal discrepancies, whereas the NMAD and the square root of the BwMv as a robust measure of the sample dispersion; instead, the mean and the standard deviation [55,56]. As a result, students learn about the non-gaussian statistics and their impact on the final results.

Please note that, for asymmetric distribution, will not be possible to provide a plus-minus range, therefore an absolute inter-percentile range at multiple confidence intervals will be provided (50% also known as the interquartile range, 90%, and 99%), and additionally some percentile values such as 2.5%, 25%, 75%, and 97.5%).

Table 4 presents the parametric and non-parametric statistical results for the façade (Figure 7a). In the table are listed the individual effects as well as the combined effect of all considered field data acquisition parameters. Please note that, for the present case, the small variation of all parameters shown in Table 3 can generate a temperature discrepancy circa 0.75 degC (median value) for the façade. Through this kind of analysis, students can assess for each 3D thermograph the effect of the individual error sources in relation to the nature of the study object. In the case of a painted brick façade, and the parameters shown in Table 4, the humidity is not a significant one; similarly, the distance due to the short range, and therefore the atmospheric effect. The more significant dispersion generated in the thermographic data is due to the material emissivity ($\pm$0.088 degC). In this case, the emissivity values are in the range of the recommended ones by the literature (Table 4). Therefore, it is shown how for this low-temperature case this effect can overpass the rest for
an area of mixed material. Parallely, the parameters which generated the higher bias in the temperature are the emissivity and ambient temperature parameters. This is an example for the engineering students about advanced statistical concepts like the central tendency (median) and dispersion (e.g., NMAD).

Table 4. Robust statistical analysis of the thermal discrepancies of the façade (degC).

| Case             | Mean   | Std.   | Median | NMAD  | Sqrt (BwMv) | P 2.5% | P 5%  | Q 25% | Q 75%  | P 95%  | P 97.5% |
|------------------|--------|--------|--------|-------|-------------|--------|-------|-------|--------|--------|---------|
| Ambient T.       | 0.142  | ±0.012 | 0.141  | 0.007 | ±0.009      | 0.120  | 0.123 | 0.136 | 0.147  | 0.160  | 0.164   |
| Humidity         | −0.010 | ±0.009 | −0.011 | 0.006 | ±0.007     | −0.027 | −0.025 | −0.014 | −0.006 | 0.004  | 0.007   |
| Distance         | −0.008 | ±0.008 | −0.009 | 0.004 | ±0.006     | −0.022 | −0.021 | −0.012 | −0.005 | 0.003  | 0.006   |
| Emisivity        | 0.121  | ±0.117 | 0.133  | 0.074 | ±0.088     | −0.085 | −0.044 | 0.077 | 0.178  | 0.316  | 0.334   |
| Reflected T.     | 0.252  | ±0.006 | 0.251  | 0.003 | ±0.004     | 0.243  | 0.244 | 0.249 | 0.254  | 0.259  | 0.260   |
| All Params.      | 0.751  | ±0.080 | 0.759  | 0.050 | ±0.060     | 0.611  | 0.638 | 0.721 | 0.790  | 0.884  | 0.896   |

The above table (Table 4) shows how a modification of the field variables will cause a modification of the façade temperature in a heterogeneous way. This discrepancy will be significant or not according to the final objective of the thermal inspection, which is governed by the teaching subject. Observe that both Figure 9 and Table 4 are only a sample of the proposed activity, which can easily be applied to any other object and/or scenario.

Additional multiple values can be derived as the interpercentile ranges (robust and/or Gaussian) for different confidence values (Table 5). These additional results allow the student to compare the effect of the Gaussian hypothesis in the analysis results.

Table 5. Robust interpercentile ranges (IPR) and Gaussian confidence intervals (CI) for the façade thermal discrepancies (degC).

| Case             | IQR      | IPR 68.27% | IPR 90%  | IPR 95%  | IPR 99%  | CI 95%  | CI 99%  |
|------------------|----------|------------|----------|----------|----------|--------|--------|
| Ambient T.       | 0.011    | 0.017      | 0.037    | 0.044    | 0.091    | 0.048  | 0.063  |
| Humidity         | 0.008    | 0.013      | 0.029    | 0.034    | 0.069    | 0.037  | 0.048  |
| Distance         | 0.007    | 0.011      | 0.024    | 0.028    | 0.059    | 0.031  | 0.041  |
| Emisivity        | 0.101    | 0.162      | 0.360    | 0.419    | 0.871    | 0.460  | 0.605  |
| Reflected T.     | 0.005    | 0.007      | 0.015    | 0.017    | 0.038    | 0.019  | 0.026  |
| All Params.      | 0.069    | 0.111      | 0.246    | 0.285    | 0.592    | 0.313  | 0.412  |

The Gaussian 99% confidence interval underestimated the robust values by approximately 30% for the present example. For the 95% CI, there is an overestimation of about 10%. This is an example of the teaching of transversal statistical competences for future professionals.

The same virtual material can be segmented into areas of interest for further analysis of the effects of the different uncertainty sources individually or combined (Figure 10); for example, for the windows where the heat exchange is more significant. Applying the same statistical analysis over the signed thermal discrepancies can be obtained in the summary shown in Table 6.

![Figure 10. Discrepancies in superficial temperature caused by the parameters’ errors for the detail area.](image-url)
Table 6. Robust statistical analysis of the thermal discrepancies of the detail area (degC).

| Case          | Mean ± Std. | Median   | NMAD ± Std. | Sqrt (BwMv) ± Std. | P 2.5% | P 5% | Q 25% | Q 75% | P 95% | P 97.5% |
|---------------|-------------|----------|-------------|--------------------|--------|-----|-------|-------|-------|---------|
| Ambient T.    | 0.146 ± 0.008 | 0.145 ± 0.007 | ±0.008 | ±0.135 ± 0.140 | 0.151  |
| Humidity      | −0.007 ± 0.006 | 0.006 ± 0.006 | ±0.006 | −0.015 ± 0.011 | −0.003  |
| Distance      | −0.006 ± 0.005 | 0.006 ± 0.006 | ±0.006 | −0.013 ± 0.010 | −0.002  |
| Emissivity    | 0.083 ± 0.074 | 0.091 ± 0.077 | ±0.077 | 0.036 ± 0.142 | 0.184   |
| Reflected T.  | 0.253 ± 0.003 | 0.253 ± 0.003 | ±0.003 | 0.249 ± 0.251 | 0.259   |
| All Params.   | 0.725 ± 0.051 | 0.730 ± 0.053 | ±0.053 | 0.628 ± 0.693 | 0.794   |

Comparing Tables 4 and 6 it is shown that the standard deviation is reduced circa 37% for the detailed area in relation to the complete façade (e.g., 0.080 degC vs. 0.051 degC). However, as shown by the square root of BwMv, this difference is about 11% (e.g., 0.060 degC vs. 0.053 degC). In absolute terms, the thermal difference can be considered no significant, but for the acquisition of competences is relevant, especially for the high-temperature cases, where these discrepancies will be magnified. Real-world data does not usually behave as the parametric models, so the robust statistic will provide correct results even if the conditions are not met exactly. This kind of mathematical skills is very valuable for future professionals to carry out accurate statistical predictions.

Similarly, in Table 7 are shown the robust and Gaussian interpercentile ranges for different confidence values.

Table 7. Robust interpercentile ranges (IPR) and Gaussian confidence intervals (CI) for the thermal discrepancies of the detail area (degC).

| Case          | Robust       | Gaussian     |
|---------------|--------------|--------------|
|               | IQR | IPR 68.27% | IPR 90% | IPR 95% | IPR 99% | CI 95% | CI 99% |
| Ambient T.    | 0.011 | 0.018 | 0.025 | 0.026 | 0.029 | 0.030 | 0.040 |
| Humidity      | 0.008 | 0.014 | 0.019 | 0.020 | 0.022 | 0.023 | 0.031 |
| Distance      | 0.008 | 0.012 | 0.016 | 0.017 | 0.019 | 0.030 | 0.026 |
| Emissivity    | 0.106 | 0.174 | 0.240 | 0.250 | 0.271 | 0.292 | 0.383 |
| Reflected T.  | 0.004 | 0.007 | 0.010 | 0.010 | 0.012 | 0.012 | 0.016 |
| All Params.   | 0.072 | 0.118 | 0.164 | 0.171 | 0.184 | 0.199 | 0.261 |

For the detail area, segmented without edge points, it can be shown the effect of Gaussian and robust estimators in the confidence interval, as shown in the table, where for a 99% confidence interval, the difference of temperature discrepancies is overestimated approximately a 41% per the combined case (0.184 degC vs. 0.261 degC). Moreover, in this case, the effect is the contrary to Table 5 where the Gaussian confidence interval underestimated the values. As a result, the same dataset can be used to teach multiple didactical examples, fulfilling the economic criteria aforementioned [21,49].

4.3. Students’ Critical Thinking and Reflections

Finally, based on the statistical results, the students will carry out a reflective task for each study case, based on the results obtained during the process (see Sections 4.1 and 4.2), about the influence of the error sources and requirements of the technique taking into account the objectives of the analysis, being this reflection the meaningful result of the activity.

This reflection will help to develop the students’ critical thinking as well as to complete the acquisition of the subject’s competences. The professor will supervise this task, ensuring the training, and the fulfilling of the learning objectives. In order to encourage the students’ reflection, the session will start with a set of open examples of questions related to the methodology. Next, and in order to illustrate them, there are exemplified some questions:

- What are the key objects of the scenario that I have to document?
- What is the objective of the final inspection report?
• Is it enough to consider the mean and standard deviation to interpret the data?
• What statistical parameters are needed to quantitatively assess sources of error?
• What are the probable field and meteorological conditions?
• What is the anticipated temperature range to be recorded?
• Do I need additional instrumentation to ensure adequate quantitative thermographic results? (for example, a thermocouple, a hygrometer).
• What should be the frequency of inspection? (number of images and temporal interval).

As a result, there will be a reinforcement of additional skills, as for example critical thinking, statistical concepts, decision making, and problem-solving. Besides, the students will learn the benefits of using software from other disciplines, as geomatics engineering, and to adapt to their needs. Students could also fulfill a table (Table 8) similar to the next one, obtained from [39]:

| Parameter                  | Influence in the Final Temperature                                           |
|----------------------------|--------------------------------------------------------------------------------|
| Object emissivity          | Sample emissivity is constant—difficult to obtain accurate values            |
| Relative humidity          | Greater variations in humidity increase uncertainty in reading               |
| Object distance            | Changes in distance will move ROI and alter camera focus                     |
| Reflected temperature      | If the background temperature is very different than the measured surface, the effect will be more significant |
| Atmosphere temperature     | Greater variations in temp. increase uncertainty in readings                  |

5. Conclusions

A procedure for thermographic image analysis using geomatic software has been presented. This procedure allows a more critical evaluation of the parameters involved in thermography and applies to the models’ statistical processing that allows seeing the distribution of data and the presence of biases or non-normalities. The research has been implemented using open software, and the activity can be integrated into e-learning or b-learning educational programs.

As a result of the pandemic situation, the number of programs available online in higher education is growing, but it remains a challenge to generate quality learning materials to transform traditional teaching into new degrees, focusing on case studies and meaningful career-related activities. In particular, the focus of this manuscript is to contribute to the creation of a series of participatory activities in subjects associated with IR imaging to stimulate critical thinking in students, in relation to the IR error sources and their consequences and variability. Collaterally, mathematical and statistical skills are also reinforced.

The final objective of this manuscript is to introduce a dynamic and comprehensive pipeline for the acquisition and development of advanced skills derived from the use of thermographic images as 3D models and the knowledge of the main sources of uncertainty. With this activity students can be introduced to the physical phenomena of heat transfer using thermography, as it has been proposed in other works at different educational levels [15,16]. Specifically, this work proposes the use of robust statistics applied on thermographic images with geomatic techniques that, as the results show, can ‘unmask’ false results derived from the application of classical parametric statistics and this can be used as a teaching potential.

Furthermore, the proposed method is low cost by emphasizing the use of open/free Geomatics software (CloudCompare) for visualization purposes and mathematical package for the mathematical conversion (Octave), both free, and that can be used both in engineering science programs, and by the student himself; unlike the infrared camera, which if it is a piece of expensive equipment, but as it is only necessary to collect the thermal images of the objects of interest to the subject. Please note, that there are also low-cost thermal imaging devices that can be used paired to a smartphone as an acceptable substitute.
The present analysis of thermographic images is highly specialized, being especially useful for engineering students familiar with rescaling of thermographic images and statistical analysis. Moreover, the activity will be specifically designed to show the importance of robust statistics and to show the student the limitations of the parametric statistics that they commonly use in other tasks. The shown case study is the monitoring of a facade for the study of heat distribution and thermal bridges. However, this methodology would be applicable to any thermographic image used in inspection and maintenance tasks (e.g., electrical systems, engines, fluid installations, etc.). As the radiation comes from the object and different sources, outliers can appear, which implies that students are only able to extract a general opinion. So, the possible presence of systematisms, and/or outliers detected in the experiments carried out, will hinder the use of Gaussian statistics like the mean and the standard deviation, since they will not always provide a suitable analysis, therefore the transversal statistical competence will benefit students’ critical thinking.

Given the multidisciplinary and novel nature of the infrared thermography technique, its experimental application could be included in different engineering programs, by explaining and understanding abstract theoretical concepts in class as well as e-learning methods, thus helping students to be better prepared to face the challenges of the Industry 4.0. Furthermore, this resource can be integrated within e-learning and b-learning methodologies.

Once it has been demonstrated the possibility of working with 3D models obtained from thermal imaging and with robust statistics in order to detect and evaluate possible errors, future works could include the experimental application of this technique in students from different engineering programs, given the multidisciplinary nature of the thermographic technique.

Author Contributions: Conceptualization, P.R.-G. and M.R.-M.; methodology, P.R.-G. and M.R.-M.; software, P.R.-G.; validation, P.R.-G. and M.R.-M.; formal analysis, P.R.-G. and M.R.-M.; investigation, P.R.-G. and M.R.-M.; resources, P.R.-G.; writing—original draft preparation, P.R.-G. and M.R.-M.; writing—review and editing, P.R.-G. and M.R.-M.; visualization, P.R.-G. and M.R.-M. All authors have read and agreed to the published version of the manuscript.

Funding: This research was partially funded by the University of Leon by the research grant No. 2018/00188/00.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Please refer to suggested Data Availability Statements in section “MDPI Research Data Policies” at https://www.mdpi.com/ethics.

Conflicts of Interest: The authors declare no conflict of interest.

References
1. Rodríguez-González, P.; Rodríguez-Martín, M. Understanding Uncertainties in Thermographic Imaging. In Proceedings of the Seventh International Conference on Technological Ecosystems for Enhancing Multiculturality (TEEM’19), León, Spain, 16–18 October 2019; pp. 65–71. [CrossRef]
2. Gaussorgues, G.; Chomet, S. Infrared Thermography; Springer: Berlin, Germany, 2012.
3. González-Aguilera, D.; Lagela, S.; Rodríguez-González, P.; Hernández-López, D. Image-based thermographic modeling for assessing energy efficiency of buildings façades. Energy Build. 2013, 65, 29–36. [CrossRef]
4. Gesto-Diaz, M.; Tombari, F.; Gonzalez-Aguilera, D.; Lopez-Fernandez, L.; Rodriguez-Gonzalez, P. Feature matching evaluation for multimodal correspondence. ISPRS J. Photogramm. Remote Sens. 2017, 129, 179–188. [CrossRef]
5. Osornio-Rios, R.A.; Antonino-Daviu, J.A.; de Jesus Romero-Troncoso, R. Recent industrial applications of infrared thermography: A review. IEEE Trans. Ind. Inform. 2018, 15, 615–625. [CrossRef]
6. Ghahramani, A.; Castro, G.; Karvigh, S.A.; Becerik-Gerber, B. Towards unsupervised learning of thermal comfort using infrared thermography. Appl. Energy 2018, 211, 41–49. [CrossRef]
7. Wilkesmann, M.; Wilkesmann, U. Industry 4.0—Organizing routines or innovations? Vine J. Inf. Knowl. Manag. Syst. 2018, 48, 238–254. [CrossRef]
8. Stachová, K.; Papula, J.; Stacho, Z.; Kohnová, L. External partnerships in employee education and development as the key to facing industry 4.0 challenges. Sustainability 2019, 11, 345. [CrossRef]
9. Piccialli, F.; Bessis, N.; Jung, J.J. Data Science challenges in Industry 4.0. IEEE Trans. Ind. Inform. 2020, 16, 5924–5928. [CrossRef]
10. Karakose, M.; Yaman, O. Complex Fuzzy System Based Predictive Maintenance Approach in Railways. IEEE Trans. Ind. Inform. 2020, 16, 6023–6032. [CrossRef]
11. Rodríguez-Martín, M.; Fueyo, J.G.; Gonzalez-Aguilera, D.; Madruga, F.J.; Garcia-Martín, R.; Muñoz, A.L.; Pisonero, J. Predictive Models for the Characterization of Internal Defects in Additive Materials from Active Thermography Sequences Supported by Machine Learning Methods. Sensors 2020, 20, 3982. [CrossRef]
12. Villa, E.; Arteaga-Marrero, N.; Ruiz-Alzola, J. Performance Assessment of Low-Cost Thermal Cameras for Medical Applications. Sensors 2020, 20, 1321. [CrossRef]
13. Barbón, A.; Barbón, N.; Otero, J.A.; Ruiz, M.M. Problemática del aprovechamiento de resultados de investigación en la docencia universitaria. In Proceedings of the XII Congreso Universitario de Innovación Educativa en las Enseñanzas Técnicas, Barcelona, Spain, 26 July 2004.
14. Diuafin Flethes, A. Diseño e Implantación de una Plataforma de Registro de Datos en Tiempo Real en Prácticas de Termodinámica y Transmisión de Calor e Ingeniería Térmica I. Bachelor’s Thesis, University of Vigo, Vigo, Spain, 2018.
15. de Prada Pérez de Azpeitia, F. La termografía infrarroja: Un sorprendente recurso para la enseñanza de la física y la química. Rev. Eureka Sobre Enseñanza Divulg. Cienc. 2016, 13, 617–627.
16. Cabello, R.; Navarro-Esbri, J.; Ilopis, R. Infrared Thermography as a Useful Tool to Improve Learning in Heat Transfer Related Subjects. Int. J. Eng. Educ. 2006, 22, 373–380.
17. Carpineti, M.; Cazzaniga, L.; Perotti, L.; Giliberti, M.; Cavinato, M.; Ludwig, N. Embedding physics into technology: Infrared thermography and building inspection as a teaching tool—a new participated strategy approach to the physics of heat transfer and energy saving for professional schools. Can. J. Phys. 2019, 97, 1019–1026. [CrossRef]
18. Ferreira, M.E.; André, A.C.; Pitarma, R. Potentialities of Thermography in Ecocentric Education of Children: An Experience on Training of Future Primary Teachers. Sustainability 2019, 11, 2668. [CrossRef]
19. Pitarma, R.; Crisóstomo, J.; Ferreira, M.E. Learning About Trees in Primary Education: Potentiality of IRT Technology in Science Teaching. In Proceedings of the EDULEARN18 Conference, Palma de Mallorca, Spain, 2-4 July 2018; pp. 208–213.
20. Heradio, R.; Torre, L.; Galán, D.; Cabrero, F.J.; Herrera-Viedma, E.; Dormido, S. Virtual and remote labs in education: A bibliometric analysis. Comput. Educ. 2016, 98, 14–38. [CrossRef]
21. Vergara, D.; Rodríguez-Martín, M.; Rubio Cavero, M.P.; Ferrer Marin, J.; Nuñez Garcia, F.J.; Moralejo Cobo, L. Formación de personal técnico en ensayos no destructivos por ultrasonidos mediante realidad virtual. Dyna 2018, 93, 150–154. [CrossRef]
22. Rossiter, J.A. Low production cost virtual modelling and control laboratories for chemical engineering students. IFAC-PapersOnLine 2016, 49, 230–235. [CrossRef]
23. Rodríguez-Martín, M.; Rodríguez-Gonzálvez, P. Materiales formativos 3D desde ingeniería inversa para el aprendizaje de la inspección de soldaduras. Dyna 2019, 94, 238–239. [CrossRef]
24. Blanco, E.; Schirmbeck, F.; Costa, C. Vocational Education for the Industrial Revolution. In International Conference on Remote Engineering and Virtual Instrumentation; Springer: Berlin/Heidelberg, Germany, 2018; pp. 649–658. [CrossRef]
25. Fox, M.; Coley, D.; Goodhew, S.; De Wilde, P. Thermography methodologies for detecting energy related building defects. Renew. Sustain. Energy Rev. 2014, 40, 296–310. [CrossRef]
26. British Standards Institute. Thermal Performance of Buildings—Qualitative Detection of Thermal Irregularities in Building Envelopes—Infrared Method; BS EN 13187:1998; BS: London, UK, 1998.
27. International Organization for Standardization. Performance of Buildings by Infrared Methods—Part 3: Qualifications of Equipment Operators, Data Analysts and Report Writers; ISO 6781-3:2015; ISO: Geneva, Switzerland, 2015.
28. International Organization for Standardization. Thermal Bridges in Building Construction—Linear Thermal Transmittance—Simplified Methods and Default Values; ISO 14683-2017; ISO: Geneva, Switzerland, 2017.
29. American Society for Testing Materials. Standard Practice for Minimum Detectable Temperature Difference for Thermal Imaging Systems; ASTM E1311; American Society for Testing Materials: West Conshohocken, PA, USA, 2018.
30. Milovanović, B.; Banjad Pečur, I. Review of active IR thermography for detection and characterization of defects in reinforced concrete. J. Imaging 2016, 2, 11. [CrossRef]
31. Kylili, A.; Fokaides, P.A.; Christou, P.; Kalogirou, S.A. Infrared thermography (IRT) applications for building diagnostics: A review. Appl. Energy 2014, 134, 531–549. [CrossRef]
32. Lucchi, E. Applications of the infrared thermography in the energy audit of buildings: A review. Renew. Sustain. Energy Rev. 2018, 82, 3077–3090. [CrossRef]
33. Pitarma, R.; Crisóstomo, J.; Jorge, L. Analysis of Materials Emissivity Based on Image Software. In Proceedings of the World-CIST’16 Conference—4th World Conference on Information Systems and Technologies, Recife, Brazil, 22–24 March 2016; pp. 749–757.
34. Rodríguez-Martín, M.; Laguela, S.; González-Aguilera, D.; Díaz-Vilarino, L. Termografía activa, parte 1: Enfoque teórico de la captación infrarroja, procesamiento de datos y clasificación. Dyna 2015, 90, 456–460. [CrossRef]
35. Fluke Corporation. Qualitative vs. Quantitative Inspections. Available online: https://dam-assets.fluke.com/s3fs-public/253439 4_b_eng_w.pdf (accessed on 28 December 2020).

36. Simpson, R.C.; McEvoy, H.C.; MacHin, G.; Howell, K.J.; Naeem, M.; Plassmann, P.; Ring, F.J.; Campbell, P.A.; Song, C.; Pavener, J.P.; et al. In-field-of-view thermal image calibration system for medical thermography systems. Int. J. Thermophys. 2008, 29, 1123–1130. [CrossRef]

37. Minkina, W.; Dudzik, S. Infrared Thermography: Errors and Uncertainties; John Wiley & Sons: Hoboken, NJ, USA, 2009.

38. Lillesand, T.; Kiefer, R.W.; Chipman, J. Remote Sensing and Image Interpretation; John Wiley & Sons: Hoboken, NJ, USA, 2015.

39. Grenyer, A.; Addepalli, S.; Zhao, Y.; Oakey, L.; Erkoyuncu, J.A.; Roy, R. Identifying challenges in quantifying uncertainty: Case study in infrared thermography. Procedia CIRP 2018, 73, 108–113. [CrossRef]

40. Bureau International des Poids et Mesures (BIPM); International Federation of Clinical Chemistry and Laboratory Medicine (IFCC); International Union of Pure and Applied Chemistry (IUPAC); International Organization for Standardization (ISO). The International Vocabulary of Metrology—Basic and General Concepts and Associated Terms (VIM), 3rd ed.; Joint Committee for Guides in Metrology (JCGM) 200; 2012. Available online: https://www.bipm.org/utils/common/documents/jcgm/JCGM_200_2012.pdf (accessed on 28 December 2020).

41. Rodríguez-Gonzálezu, P.; Rodríguez-Martínu, M.; Alonso-Cortés Fradexab, B.; Alvearb-Ordenes, I. 3D Visualization Techniques in Health Science Learning. Application case of Thermographic Images to Blood Flow Monitoring. In Proceedings of Sixth International Conference on Technological Ecosystems for Enhancing Multiculturality (TEEM’18), Salamanca, Spain, 24–26 October 2018; pp. 373–380. [CrossRef]

42. Marqués-Sánchez, P.; Liébana-Presac, C.; Benítez-Andradas, J.A.; Gandín-Gallelog, R.; Álvarez-Barrío, L.; Rodríguez-González, P. Thermal Infrared Imaging to Evaluate Emotional Competences in Nursing Students: A First Approach through a Case Study. Sensors 2020, 20, 2502. [CrossRef]

43. Harvey, P. ExifTool: Read, Write and Edit Meta Information. Available online: https://exiftool.org/ (accessed on 28 December 2020).

44. Eaton, J.W.; Bateman, D.; Hauberg, S. GNU Octave Manual; Network Theory Ltd.: Bristol, UK, 2002.

45. Gilchrist, W.G. Statistical Modelling with Quantile Functions; Chapman and Hall/CRC: London, UK, 2000.

46. Rodríguez-González, P.; García-Gago, J.; Gomez-Lahoz, J.; González-Aguilera, D. Multispectral Radiometric Analysis of Façades to Detect Pathologies from Active and Passive Remote Sensing. Remote Sens. 2016, 8, 80. [CrossRef]

47. Höhle, J. The assessment of the absolute planimetric accuracy of airborne laser scanning. Int. Arch. Photogramm. Remote Sens. Spat. Inf. Sci. 2011, 1145–150. [CrossRef]

48. Nocerino, E.; Menna, F.; Remondino, F.; Toschi, I.; Rodríguez-González, P. Investigation of indoor and outdoor performance of two portable mobile mapping systems. In Proceedings of the Videometrics, Range Imaging, and Applications XIV, Munich, Germany, 26 June 2017; Volume 10332, p. 103320I. [CrossRef]