We discuss the nuclear parton distribution functions on the basis of our recently developed semi-microscopic model, which takes into account a number of nuclear effects including Fermi motion and nuclear binding, nuclear meson-exchange currents and off-shell corrections to bound nucleon distributions as well as nuclear shadowing effect. We also discuss application to the nuclear Drell-Yan process and compare our predictions with data from the E772 and E866 experiments.
1. Introduction

The parton distributions (PDFs) are universal process-independent characteristics of the target at high invariant momentum transfer $Q$, which determine the leading contributions to the cross sections of various hard processes involving leptons and hadrons. The nuclear parton distributions (nPDFs) are the subject of significant nuclear effects which span a wide region of Bjorken $x$ with a rate more than one order of magnitude larger than the ratio of the nuclear binding energy to the nucleon mass (for a review see [1, 2]). These observations indicate that the nuclear environment plays an important role even at energies and momenta much higher than those involved in typical nuclear ground state processes.

A few phenomenological approaches to nPDFs are available in literature [3, 4, 5, 6]. Although such studies are useful in constraining nuclear effects for different partons, they provide little information about the underlying physics mechanisms responsible for the nuclear corrections. In this contribution we follow a different approach and present the results of a study of nPDFs using a semi-microscopic model of Ref.[7]. The model accounts for a number of nuclear corrections including the smearing with the energy-momentum distribution of bound nucleons (Fermi motion and binding, or FMB), the off-shell correction (OS) to bound nucleon structure functions, the contributions from meson exchange currents (MEC), and the effects of propagation of the hadronic component of the virtual intermediate boson in the nuclear environment. The model quantitatively explains the observed $x$, $Q^2$ and $A$ dependencies of the nuclear structure functions in the deep-inelastic scattering (DIS) for a wide range of nuclear targets from $^3$H to $^{207}$Pb [7, 8, 9]. Here we discuss the region of high $Q$ and address the predictions of the model for nPDFs and the nuclear Drell-Yan (DY) process (see Ref.[10] for more detail).

2. Outline of a model

We will use the notation $q_{a/T}(x,Q^2)$ for the distribution of quarks of the flavor $a$ in a target $T$. The parton distributions in a nucleus receive a number of contributions and can be written as [7, 10] (for brevity, we suppress explicit dependencies on $x$ and $Q^2$):

$$q_{a/A} = \langle q_{a/p} \rangle + \langle q_{a/n} \rangle + \delta q_a^{coh} + \delta q_a^{MEC}. \tag{2.1}$$

The first two terms on the right side are the contribution from the partons from bound protons and neutrons averaged with the nuclear spectral function, as discussed in detail in Ref.[7, 10]. Note that the evaluation of these terms requires the proton and the neutron PDFs in off-mass shell region [11]. The off-shell correction together with the nucleon momentum distribution (Fermi motion) and the nuclear binding effect [12] plays an important role in the valence quark region [7, 9].

The $\delta q^{coh}$ correction is relevant at low $x$ and arises due to propagation effects of intermediate hadronic states of a virtual boson in nuclear environment. This term involves contributions from multiple scattering series and typically lead to a negative correction (nuclear shadowing effect, for a review see, e.g., Ref.[13]).

The last term in Eq.(2.1) is a contribution from the pion (as well as the other meson) degrees of freedom in nuclei. This term is relevant for intermediate region of $x$ and results in a some enhancement of the nuclear sea quark distribution. Also its contribution is important to balance the...
overall nuclear light-cone momentum. More details on the treatment of each term in Eq. (2.1) can be found in Refs. [7, 10]. Below we summarize our results on the nuclear valence and sea quark PDFs.

3. Results

Figure 1 displays the ratios \( R_a = q_a/A/(Zq_{a/p} + Nq_{a/n}) \) for the valence quarks (left panel) and the antiquarks (right panel) in \(^{208}\text{Pb}\) calculated at \( Q^2 = 25\text{GeV}^2 \) (see text for more detail). Figure 1: (Color online) The nuclear ratios for the valence quarks (left panel) and the \( \bar{u}, \bar{d}, \) and \( \bar{s} \) antiquarks (right panel) in \(^{208}\text{Pb}\) calculated at \( Q^2 = 25\text{GeV}^2 \) (see text for more detail).

and also depends on the PDF flavor. We briefly comment on characteristic features of the nuclear ratios for different PDFs, for a more detail discussion see Ref. [10].

In the region \( x \ll 0.1 \), all nPDFs are suppressed due to the nuclear shadowing effect (the \( \delta q^{\text{coh}} \) term). Note that this effect is not universal and differs for the valence and sea quark distribution [7, 10].\(^1\) We also remark that the result of averaging of the nucleon PDF with nuclear spectral function [the FMB effect, see the first two terms in the right side of Eq. (2.1)] depends on the details of the \( x \) dependence of considered PDF. In particular, the combined FMB and OS correction at small \( x \) is positive for the valence quark and negative for the sea quark and gluon PDFs.

In the intermediate region of \( x \sim 0.1 \) (which is usually referred to as antishadowing region) we observe interplay between different nuclear corrections. For the valence quark PDF (C-odd \( q^- \) distribution) we find an enhancement which is due to constructive interference in the multiple scattering effect between the C-even and C-odd amplitudes in the \( \delta q^{\text{coh}} \) term. The antishadowing effect on the antiquark PDFs is significantly weaker because of a partial cancellation between different contributions. We also note that, unlike the \( \bar{u} \) and \( \bar{d} \), the nuclear \( \bar{s} \) in Fig.1 does not include the MEC term.

\(^1\)In our analysis we choose the PDFs with definite C-parity \( q^= = q \pm \bar{q} \) as a basis. The C-odd \( xq^- \) and the C-even \( xq^+ \) distributions correspond to the structure function \( xF_3 \) and \( F_2 \), respectively. For light quarks we also consider the isoscalar \( q_0 = u + d \) and the isovector \( q_1 = u - d \) combinations. As was noticed in Ref. [14], the relative shadowing effect for \( F_3 \) (or \( q^- \)) is enhanced by the factor of 2 of that of \( F_2 \) if the real parts of effective scattering amplitudes vanish. The presence of the real parts leads to important interference effect thus reducing the shadowing effect [7, 10].
At large \( x > 0.2 \) the nuclear corrections are dominated by the FMB and OS corrections. For the valence quarks, those corrections form a pronounced ‘EMC-effect’ shape at large \( x \) [7]. However, as was mentioned above, the FMB correction crucially depends on the \( x \) shape of the PDF and for this reason is different for antiquark distribution.

Figure 2 displays the ratios of the Drell-Yan (DY) reaction cross sections as a function of the target’s Bjorken variable \( x_T \), which were calculated for the targets and the kinematics of E772 [15] and E866 [16] experiments. The nuclear dependence of the DY process comes from two different sources: (i) the modification of the nuclear target PDFs, and (ii) the initial state interaction of the projectile particle (parton) within the nuclear environment of the target.

Note that for the E772 and E866 kinematics the DY nuclear ratios in the region \( x_T < 0.15 \) are driven by the ratios of the antiquark distributions in the corresponding targets. We recall that the lack of antishadowing in the DY data at \( x \sim 0.1 \) was a long standing puzzle since the nuclear binding should result in an excess of nuclear mesons, which is expected to produce a marked enhancement in the nuclear anti-quark distributions [19]. As discussed above, our model predicts a significant cancellation of different nuclear effects in the antiquark distribution in the region \( x \sim 0.1 \) in agreement with the nuclear DY data.

The projectile partons in the initial state can undergo multiple soft collisions in nuclear medium.
and radiate gluons thus loosing the energy [17] before annihilating with the (anti)quarks of the target and producing a dimuon pair. In order to account for the quark energy loss effect, let $E'$ be the parton energy loss in a nucleus per unit length. If a projectile parton travels over the distance $L$ in the nuclear environment before annihilation, then its Bjorken variable $x_B$ changes by $E'L/E_p$, where $E_p$ is the energy of the projectile proton (see, e.g., Ref.[18]). We estimate the average propagation length of the projectile partons in the uniform nuclear medium as $L = 3R/4$, where $R$ is the nucleus radius. Our analysis [10] indicates that the E772 and E866 data favor the presence of a moderate energy loss effect. The solid curves in Fig.2 show our predictions with $E' = 0.7 \text{ GeV/fm}$.

The data from the E866 experiment is shifted towards lower values of target's $x_T$ and higher values of projectile's $x_B$ with respect to E772 data, as can be seen from Fig.2. The kinematic coverage of E866 data is therefore focused on the region where both shadowing and energy loss effects become more prominent. The E866 data are consistent with the E772 data in the overlap region. Figure 2 shows that our predictions for the E866 and E772 kinematics are in good agreement data. We also note that the E866 and E772 experiments present somewhat different nuclear ratios: $A/^{2}_H$ in the case of E772 and $A/^{9}_Be$ in the case of E866. For this reason the corresponding curves in Fig.2 do not coincide in the E866–E772 overlap region.

4. Summary

In summary, we presented the results of our studies [10] of nPDFs basing on an approach which was successfully applied to nuclear DIS in Refs.,[7, 9]. A number of mechanisms responsible for nuclear corrections on PDFs in different regions of Bjorken $x$ was discussed. We also discussed the application to the nuclear DY process and found that our predictions on the ratio of the DY yields are in a good agreement with the measurements by the E772 and E866 experiments. We also studied the sensitivity of the nuclear DY reaction to the energy loss effect of the projectile parton in nuclear environment, the effect which is not included in phenomenological nPDF analyses.

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