Coulomb distortion in the inelastic regime

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Abstract. The Coulomb distortion effects have been for a long time neglected in deep inelastic scattering for the good reason that the incident energies were very high. But for energies in the range of earlier data from SLAC or at JLab, the Coulomb distortion could have the potential consequence of affecting the A-dependence of the EMC effect and of the longitudinal to transverse virtual photon absorption cross section ratio $R(x, Q^2)$.

Keywords: Deep inelastic scattering, Coulomb distortion, nuclear dependence, EMC effect

PACS: 13.60.Hb, 25.30.Fj, 24.85.+p

INTRODUCTION

The incident (scattered) electron is accelerated (decelerated) due to the Coulomb field created by the nearby protons through the exchange of soft photons. The Coulomb distortion manifests when the electromagnetic interaction is used to probe the nucleus and its effect increases with the number ($Z$) of protons inside the nucleus. The effect is expected to have the opposite sign with a positron beam.

Due to these changes in the initial and final kinematics and the wavefunctions of the lepton, the cross sections cannot be expressed by the Plane Wave Born Approximation (PWBA); the Distorted Wave Born Approximation (DWBA) should be considered instead. However full calculation of DWBA is very extensive and difficult to implement. A more convenient approach is the Effective Momentum Approximation (EMA) where the incident and scattered electron energies ($E$ and $E_p$, respectively) are shifted by an average Coulomb potential, $\bar{V}$, seen by the electron. Moreover, a focusing on the incoming lepton plane wave needs to be applied. In Ref. [1], A. Aste and collaborators have made a detailed comparison of the EMA to a full DWBA calculation for quasi-elastic scattering. In their approach, the spectral function is subject to the transformation $S_{\text{tot}}^{\text{PWBA}}(|\vec{q}|, \omega, \theta) \rightarrow S_{\text{tot}}^{\text{EM}}(|\vec{q}_{\text{eff}}|, \omega, \theta)$, with $\omega$ and $\vec{q}$ the energy and momentum transferred to the nucleon and $\theta$ the scattering angle. The Mott cross section undergoes the transformation $\sigma_{\text{Mott}} \rightarrow \alpha^2 \cos^2(\theta/2)(E_p + \bar{V})^2/Q_{\text{eff}}^4$ with:

$$\sigma_{\text{Mott}}^{\text{eff}} = 4\alpha^2 \cos^2(\theta/2)(E_p + \bar{V})^2/Q_{\text{eff}}^4$$

with the effective squared four-momentum transfer $Q_{\text{eff}}^2$ equal to $4(E + \bar{V})(E_p + \bar{V})\sin^2(\theta/2)$, $\alpha$ the fine structure constant. Finally, the incoming focusing factor $F_{\text{foc}}^i$ is

1 This work was supported by U.S. Department of Energy, Office of Nuclear Physics, under contract numbers DE-AC02-06CH11357 and DE-AC05-84ER40150 Modification No. M175.
FIGURE 1. The EMC effect in Gold before (left plot) and after (right plot) Coulomb corrections (corrections have been applied to all data sets). The JLab E03-103 data are preliminary.

equal to \((E + \bar{V})/E\). The resulting cross section has the following form:

\[
\sigma_{cc}^{\text{tot}} = (F_{\text{ foc}}^i)^2 \cdot \sigma_{\text{Mott}}^{\text{ tot}}(q_{\text{ eff}}, \omega, \theta)
\]  

(2)

The electrostatic potential \(V(r)\) inside the charged sphere of radius \(R = 1.1A^{1/3} + 0.86A^{-1/3}\) defined as followed:

\[
V(r) = -\frac{3\alpha(Z - 1)}{2R} + \frac{\alpha(Z - 1)}{2R} \left( \frac{r}{R} \right)
\]  

(3)

where the effect of the probed proton is neglected. Because most the nucleons of heavy nuclei are located in the nucleus peripheral region, taking the electrostatic potential at the center of the nucleus will be an overestimate of the Coulomb effect. When using an effective potential \(\bar{V} \approx (0.75...0.80)V(0)\), the authors in [1] showed the good agreement of EMA with the full DWBA calculation [2]. The same effective potential value was extracted from positron and electron quasi-elastic scattering experiment [3].

IMPACT ON THE EMC EFFECT

The EMC effect was first observed at CERN when physicists decided to use heavy nuclei in order to increase the luminosity in the study of nucleon substructure. They discovered that the quark distributions are different when the nucleon is inside the nuclear medium. Many other experiments confirmed this observation, and even with more complete and precise data from SLAC E139 [4], the origin of this reduction of the high momentum quark distribution in nuclei is not yet well understood. It is widely accepted that nuclear binding and Fermi motion components must be included in realistic theoretical calculations, although they alone cannot explain the EMC effect. More exotic ideas may need to be included, e.g. nuclear pions, multiquark clusters, dynamical rescaling, etc (see Ref. [5] for a review).

New results from JLab experiment E03-103 [6] on heavy nuclei motivated us to have a more detailed look at the possible significant effect from the Coulomb distortion. Un-
fortunately there have been no detailed calculations of the Coulomb distortion in the inelastic regime for beam energies on the order of several GeV (i.e. SLAC kinematics). In particular there are no studies verifying that EMA is a good approximation in this channel. Nonetheless the EMA is a reasonable approach for making an estimate regarding the potential impact of Coulomb distortion in inelastic scattering. Using the formalism defined in the previous section, the data from E03-103 were corrected as shown in Fig. 1 for Gold. Upward shifts of about 10% and 3% are observed for the JLab E03-103 and SLAC E139 data respectively. The slight difference between the two E03-103 data sets seems to be resolved after the correction. This may indicate that the use of EMA is valid in the inelastic regime too. Note, though, that the apparent agreement between the JLab and SLAC data gets worse after corrections. This will be address in more details later. It can be clearly seen that neglecting the effect of the Coulomb field at the SLAC or JLab energies would imply an overestimate of the EMC effect in medium-weight to heavy nuclei.

From measurements of the EMC effect on a wide range of nuclei, one can extrapolate to an infinitely heavy nucleus, also called infinite nuclear matter. These results are key to our understanding of nucleon’s in-medium modification as they can be compared to exact calculations [7, 8] and avoid the complexity arising from the nuclear structure of the finite nuclei. A global analysis of the world data [9] has been performed which includes Coulomb correction. The data most sensible to this analysis are the SLAC E139 and JLab E03-103 data which were taken at relatively lower energies than CERN. Because the Coulomb distortion increases with $Z$ ($A$), their effects change the extrapolation from finite nuclei to infinite nuclear matter.

Following the same procedure as in Ref. [10], the size of the EMC effect in infinite nuclear matter was extracted at several $x$-values in order to map out its $x$-dependence. In Fig. 2 the extrapolations from the original world data and from the Coulomb corrected ones are illustrated for $x = 0.7$. A 3% difference is found between the two extrapolations. Including the preliminary Coulomb corrected data from E03-103 does not change the extrapolated value for nuclear matter. This gives us some confidence that the
Coulomb distortion method used is appropriate as well in the deep inelastic scattering regime, given the large (-10%) correction for Gold at \( x \approx 0.75 \). On a related topic, other dependences of the EMC effect are being looked at, e.g. with more involved nuclear density calculations or using the nucleon overlap distributions \([11]\).

**THE NUCLEAR DEPENDENCE OF** \( R = \sigma_L / \sigma_T \) **REVISITED**

The longitudinal to transverse virtual photon absorption cross section ratio \( R \) contains important information on the nature of the nucleon’s constituents \([5]\). If the nucleon is composed mostly of spin-1/2 partons, \( R \) (\( R \sim 4m_q^2/Q^2 \)) should be very small \((\approx 0)\) and decrease with \( Q^2 \). However, if spin-0 partons and/or correlations between partons have non-negligible contributions, \( R \) will be larger and increase with \( Q^2 \).

Measuring \( R \) for nuclear targets is of equal importance as it could shed light on the underlying physics responsible for the EMC effect. A demonstration of the nuclear independence of \( R \) would lead to the conclusion that confinement properties are the same in a free nucleon and in a bound nucleon. If a nuclear dependence would be observed, one could state that the nuclear medium is changing the contribution of the spin-0 partons and higher twist effects of the nucleon.

The most precise test of the \( A \)-dependence of \( R \) at large \( x \) was done in \([12]\). The authors found no nuclear dependence of \( R \) and therefore concluded that \( \sigma_A / \sigma_D \) can be directly used to study the nuclear dependence of the EMC ratio, which is defined as \( F_A^2 / F_D^2 \). However in the analysis of Ref. \([12]\), the Coulomb distortion effects have been assumed to be small. A re-analysis of these data including Coulomb corrections \([13]\) shows a non-trivial change of slope in the extraction of \( R_A - R_D \) (from -0.018 ± 0.055 to -0.051 ± 0.058), but being still consistent with zero within the error bar. This observation becomes even more obvious after including the data from \([4]\) and the preliminary data on Copper from JLab E03-103 (see left plot in Fig. \([3]\)), which gives us a larger lever arm.
in ε′ = ε/(1 + εRD). The value for RA − RD at x = 0.5 is then found to be -0.084 ± 0.040. The use of variable ε′ is convenient to extract the A-dependence of R as, in the case of RA = RD, σA/σD should be found constant when plotted versus ε′. Before applying the corrections, RA − RD from the same set of data was equal to -0.035 ± 0.040. In fact, Coulomb corrections are strongly ε-dependent and therefore corrupt the ε-dependence in the extraction of R in medium to heavy nuclei.

Finally, note that this apparent nuclear dependence of R explains the discrepancy between the E139 and JLab data after Coulomb corrections.

CONCLUSION

Coulomb distortion cannot any longer be considered as a low energy effect. It was shown in this paper that, for earlier SLAC experiments, the Coulomb corrections were small but not negligible. For JLab E03-103 data, the corrections can certainly not be disregarded. The agreement between the SLAC and JLab data is very good after this correction is applied and the extrapolation to infinite nuclear matter is shifted upward by about 3% relative, which is a significant effect when one wants to compare to more evolved theoretical calculations.

It is also not clear whether the longitudinal to transverse virtual photon absorption cross section ratio R is nuclear independent or not, and a more precise measurement is needed. More generally, all measurements using medium-weight to heavy nuclei are sensitive to the Coulomb distortion, and it is therefore crucial to perform measurements of the Coulomb potential in different lepton scattering regimes, which requires the direct comparison of inelastic scattering data using both electron and positron beams.

POSITRON BEAM REQUIREMENTS

A possible measurement of the Coulomb distortion in the inelastic region will require a positron beam intensity of at least 10 nA for a basic check and about 100 nA for complete and detailed measurement in a reasonable beamtime of about a week.

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