Critical behavior of the insulator-to-metal transition in Te-hyperdoped Si

Wang, M.; Debernardi, A.; Zhang, W.; Xu, C.; Yuan, Y.; Xie, Y.; Berencén, Y.; Prucnal, S.; Helm, M.; Zhou, S.;

Originally published:
August 2020

Physical Review B 102(2020), 085204

DOI: https://doi.org/10.1103/PhysRevB.102.085204

Perma-Link to Publication Repository of HZDR:
https://www.hzdr.de/publications/Publ-31476

Published on the basis of the publishers policy.
Critical behavior of the insulator-to-metal transition in Te-hyperdoped Si

Mao Wang, A. Debernardi, Wenxu Zhang, Chi Xu, Ye Yuan, Yufang Xie, Y. Berencén, S. Prucnal, M. Helm, and Shengqiang Zhou

1Helmholtz-Zentrum Dresden-Rossendorf, Institute of Ion Beam Physics and Materials Research, Bautzner Landstrasse 400, 01328 Dresden, Germany
2CNR-IMM, sede Agrate Brianza, via Olivetti 2, I-20864 Agrate Brianza, Italy
3University of Electronic Science and Technology of China, State Key Laboratory of Electronic Thin Films and Integrated Devices, 610054 Chengdu, China
4Institute for Integrative Nanosciences, Institute for Solid State and Materials Research (IFW Dresden), Helmholtzstrasse 20, 01069 Dresden, Germany
5Songshan Lake Materials Laboratory, Dongguan, Guangdong 523808, People’s Republic of China
6Technische Universität Dresden, 01062 Dresden, Germany

(Received 22 March 2020; revised 23 June 2020; accepted 7 August 2020; published 25 August 2020)

Hyperdoping Si with chalcogens is a topic of great interest due to the strong sub-band-gap absorption exhibited by the resulting material, which can be exploited to develop broadband room-temperature infrared photodetectors using fully Si-compatible technology. Here, we report on the critical behavior of the impurity-driven insulator-to-metal transition in Te-hyperdoped Si layers fabricated via ion implantation followed by nanosecond pulsed-laser melting. Electrical transport measurements reveal an insulator-to-metal transition, which is also confirmed and understood by density functional theory calculations. We demonstrate that the metallic phase is governed by a power-law dependence of the conductivity at temperatures below 25 K, whereas the conductivity in the insulating phase is well described by a variable-range hopping mechanism with a Coulomb gap at temperatures in the range of 2–50 K. These results show that the electron wave function in the vicinity of the transition is strongly affected by the disorder and the electron-electron interaction.

DOI: 10.1103/PhysRevB.102.085204

I. INTRODUCTION

The insulator-to-metal transition (IMT) in doped semiconductors is a prototypical example for a quantum phase transition and has been explored in many different systems, to a large fraction in Si doped with shallow donors or acceptors. Generally, the IMT may be controlled by an external parameter \( x \) which is experimentally accessible by impurity concentration \( (N) \), electric \( (E) \) or magnetic \( (B) \) field, or uniaxial stress \( (S) \) [1–6]. In current understanding, the IMT is driven by both disorder and interaction, thus being a mixed Anderson-Mott-Hubbard type of transition. In the simple model introduced by Mott [7], a criterion is derived relating the effective Bohr radius \( (a_B) \) of an isolated impurity with the critical density of impurities \( (n_{\text{crit}}) \) at the transition, given by \( a_B n_{\text{crit}}^{1/3} \sim 0.25 \). Experimentally, the impurity-mediated IMT has been studied extensively for shallow-level impurities (such as B, P, As, and Sb) in heavily doped Si [5,8,9], where the critical transition concentration is below the solubility limit [10,11] and in the order of \( 10^{18} \text{ cm}^{-3} \) [12].

There are very few and relatively recent experimental studies of the IMT with deep-level impurities, such as chalcogens (S, Se, and Te) in Si [13–16]. According to Mott’s theory the IMT is expected to occur at much higher concentrations \( (n_{\text{crit}} \gg 10^{18} \text{ cm}^{-3}) \) than for shallow donors, since electrons are much more tightly bound with a significantly reduced radius. In previous work chalcogen-hyperdoped Si with nonequilibrium concentrations was prepared using ion implantation followed by pulsed laser melting (PLM) [13,14,17]. In those studies, the transition from insulating to metallic conduction was identified with impurity concentrations exceeding \( 10^{20} \text{ cm}^{-3} \), which is four orders of magnitude larger than their equilibrium solubility limit of about \( 10^{15} \text{ cm}^{-3} \) [11]. Moreover, the nature of the IMT was explored by both experimental and computational approaches, where the IMT was owing to the delocalization of donor electrons above a critical donor concentration \( (n_{\text{crit}}) \) [1], which results in the formation of an intermediate band (IB) [14,18] and the merging of the broadened IB with the conduction band. A more systematic study on the conduction mechanism in the insulating and metallic phases and in the critical regime of the transition is however still lacking.

In the present work, we employ experimental and computational methods to identify the impurity-induced IMT in Si hyperdoped with Te and explore the critical behavior near the transition. We analyze the temperature-dependent conductivity of the Te-hyperdoped Si samples, which cover both sides of the insulator-to-metal transition. We find a power-law dependence in metallic samples and a variable

*Corresponding author: m.wang@hzdr.de
†Corresponding author for first-principles calculations: alberto.debernardi@mdm.imm.cnr.it
range hopping mechanism with a Coulomb gap in insulating samples. Combining with the first-principles calculations, this work provides a consistent picture about the critical Te concentration and the conductivity behavior near the IMT.

II. METHODS

A. Computational details

First-principles calculations of electronic structures were performed by plane-wave pseudopotential techniques within the framework of density functional theory (DFT) as implemented in QUANTUM ESPRESSO (QE) open-source code [19]. The simulation of hyperdoped silicon was performed by the supercell method by using ultrasoft pseudopotentials [20–22] in the separable form introduced by Kleinmann and Bylander [23], generated with a Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional. For substitutional single Te (TeSi) and substitutional Te dimer (TeSi-TeSi), after structural relaxation we computed the electronic band structure and the density of states (DOS) by solving the Kohn-Sham equations. All other computational parameters are the same as in Ref. [24] to which the interested reader can refer for further computational details. The Te concentration for both TeSi and TeSi-TeSi refers to the percent concentration of Te atoms with respect to the total amount of Si plus Te atoms. At a given concentration, to simulate TeSi or TeSi-TeSi, the size of the supercell (i.e., the total number of atomic sites) and/or the number of Te atoms in the supercell are arranged accordingly in order to obtain the stated Te concentration.

B. Experimental details

Single-side polished Si (100) wafers (intrinsic, $\rho \geq 10^4$ $\Omega$ cm) were implanted with Te ions with six different fluences (as shown in Table I) at room temperature. All Te concentrations were first calculated using the SRIM code [25] and then verified by Rutherford backscattering spectrometry (RBS) measurements (labeled in Fig. 1 and listed in Table I). A combined implantation at energies of 150 and 50 keV with a fluence ratio of 2.5:1 was applied for a relatively uniform distribution of Te in the implantation region. Subsequently, ion-implanted samples were annealed using a pulsed XeCl excimer laser (Coherent COMPexPRO201, wavelength 308 nm, pulse duration 28 ns) in ambient air. A single laser pulse with an energy density of 1.2 J/cm$^2$ was used for processing samples presented in this work. After PLM, the damaged layer is recovered and its crystalline quality is comparable to that of the virgin Si wafer [17]. Single-crystalline epitaxial regrowth of the Te-hyperdoped Si has also been confirmed by high-resolution transmission electron microscopy. Moreover, Te is found to be evenly distributed within the top 120 nm of the Si wafer without the formation of extended defects, secondary phases, or cellular breakdown [17]. During the annealing process, the whole amorphous implanted region was molten and then recrystallized with a solidification speed in the order of $10$ m/s while cooling down [26]. This condition allows for Te concentrations beyond the solid solubility limit of Te in Si while preserving the epitaxial single-crystal growth.

The electrical properties of Te-hyperdoped Si samples were examined using a commercial Lakeshore Hall System (9700A) in van der Pauw geometry [29]. Samples were measured in the temperature range from 2 to 300 K and a magnetic field perpendicular to the sample plane swept from $-5$ to $5$ T. Prior to the electrical measurements, the native SiO$_2$ layer was

| Sample ID | Tellurium concentration (N) (%) | Tellurium concentration (N) (cm$^{-3}$) |
|-----------|-------------------------------|----------------------------------------|
| Te-0.39%  | 0.39                          | $1.95 \times 10^{20}$                  |
| Te-0.92%  | 0.92                          | $4.80 \times 10^{20}$                  |
| Te-1.56%  | 1.56                          | $7.80 \times 10^{20}$                  |

| Sample ID | Nominal tellurium peak concentration (N) (cm$^{-3}$) | Nominal tellurium peak concentration (N) (%) | Measured carrier concentration at 300 K (n) (cm$^{-3}$) |
|-----------|-----------------------------------------------------|---------------------------------------------|----------------------------------------------------------|
| Te-0.25%  | $1.25 \times 10^{20}$                               | 0.25                                        | $2.0 \times 10^{19}$                                       |
| Te-0.50%  | $5.00 \times 10^{20}$                               | 1.00                                        | $4.4 \times 10^{20}$                                       |
| Te-1.00%  | $7.50 \times 10^{20}$                               | 1.50                                        | $6.0 \times 10^{20}$                                       |
| Te-1.50%  | $1.00 \times 10^{21}$                               | 2.00                                        | $8.3 \times 10^{20}$                                       |

FIG. 1. RBS random spectra (symbols) and the fit (lines) to the RBS random spectra using the SIMNRA code [27,28] of PLM-treated Te-hyperdoped Si samples. The inset shows the Te signal for all samples where the sample names refer to the peak Te concentration.
removed by HF etching. Subsequently, gold electrodes were sputtered onto the four corners of the squarelike samples to ensure Ohmic contact [30]. Silver glue was used to contact the wires to the gold electrodes. The carrier concentrations of Te-hyperdoped Si samples obtained from the Hall effect measurements are listed in Table I, where the electrical activation efficiency of 10–40% can be deduced. In our previous work, we have found that there is a considerable amount of interstitial Te in samples with low doping concentrations. This explains the lower activation fraction for samples Te-0.25%, Te-0.5%, and Te-1.0%. However, with increasing impurity concentration, Te dopants tend to form substitutional dimers at the expense of interstitials, which provide free electrons leading to higher activation fraction.

### III. RESULTS

#### A. Band structure and DOS

In the band-structure and density-of-states (DOS) calculations of Te-hyperdoped Si we considered the Te substitutional impurities, namely substitutional single Te (Te$_{Si}$) and substitutional Te dimers (Te$_{Si}$-Te$_{Si}$), which represent the large majority of defect type present in hyperdoped Si. At the Te concentrations considered in the present study, the interstitial Te impurities exhibit a significantly higher formation energy [24]. Particularly, according to the previous study in Ref. [24], Te$_{Si}$-Te$_{Si}$ has the lowest formation energy among all types of defects considered and becomes the dominant configuration as effective donors with increasing Te concentration, especially in the metallic regime [24]. The computed electronic DOS and the electronic band structure for Te$_{Si}$ and Te$_{Si}$-Te$_{Si}$ in Te-hyperdoped Si at three different Te doping concentrations ($x = 0.39\%$, 0.92\%, and 1.56\%) are displayed in Figs. 2 and 3. The doping concentration range was chosen to basically cover the transition from the insulating to the metallic regime. In this section (Sec. III A) we present the first-principles simulations of electronic states, and in the next section (Sec. III B) the electrical conductivity measurements. The random distribution of dopants lifts the translational invariant symmetry, thus for a direct comparison of simulated electronic states with experimental data the DOS becomes the relevant quantity rather than the band structure. However, it can be convenient to study the evolution of the electronic states produced by doping, looking to the modification of the IB in the band structure obtained by the supercell method.

The calculated band structure and the DOS of Te-hyperdoped Si shown in Figs. 2 and 3 demonstrate the modification of the electronic properties and, in particular, the evolution of the IB which at low concentration is in the indirect band gap originating from the conduction-band minimum (CBM) and the valence-band maximum (VBM) of pure Si. As the concentration of Te is increased, the local CBM located at the $\Gamma$ point is pushed downward due to the interactions between Te and Si. As displayed in Figs. 2(a) and 2(b), for Te$_{Si}$ single impurities at $x = 0.39\%$, the IB is still separated from the CBM (by approximately 0.04 eV). The small gap between the CBM and the completely filled IB leads to a vanishing contribution to the conduction at lowest temperatures, since there are no nearby empty states.
Therefore, at this concentration Te-dimer-hyperdoped Si is in the insulating state and exhibits only thermally activated conductivity, being qualitatively consistent with previous experimental investigations [17,31,32].

At the concentration of $x = 0.39\%$, the IBs corresponding to Te$_{Si}$ and Te$_{Si}$-Te$_{Si}$ are relatively flat. As the Te concentration increases, the impurity band is getting broader [see Figs. 3(a)–3(d)], which indicates the increased delocalization of the impurity states. This is due to the decreased spacing between impurities, which results in the increased dispersion and interactions between neighboring Te impurities [17]. Particularly, as shown in Figs. 3(a) and 3(b), at the doping concentration $x = 0.92\%$, the IB is widened and tends to partially overlap with the CB. This band overlap produces the full hybridization of the higher-energy IB with the lower-energy conduction states. At the same time the Fermi level is no longer located in the region of the forbidden energy as for the insulating state, but gradually enters into the CB, producing a metallic state. Thus, the low-lying conduction-band-like states are available for the charge transport without thermal activation, implying the occurrence of the IMT upon doping. At Te concentrations of 1.56%, the IB is further widened to about 0.52 eV for Te$_{Si}$ and 0.40 eV for Te$_{Si}$-Te$_{Si}$ in Te-hyperdoped Si, respectively [see Figs. 3(c) and 3(d)]. Particularly, for the Te$_{Si}$-Te$_{Si}$ case there is a strong hybridization of IB with states originating from Si valence bands [more details can be found in Fig. 4(c) in Ref. [24]]. In Fig. 3, the intersection of Fermi energy level with the conduction band is a fingerprint of the overlap of higher-energy IB with lower-energy SI conduction bands, as evidenced by looking at the DOS (while this is less evident by looking at the electronic bands that are displayed along two high-symmetry directions. They only account partially for the electronic structure of the whole Brillouin zone. The latter information is contained in the DOS). The band structures and DOS analysis demonstrate the delocalization of the impurity states and the eventual merging of the IB and the CB as the doping concentration increases.

As displayed in Figs. 3(a)–3(d), the Fermi level is located in the CB for both systems at Te doping concentration of 0.92% and 1.56%, which corresponds to the metallic state and is consistent with transport measurement results (see Fig. 4). However, for the case of Te$_{Si}$-Te$_{Si}$ at $x = 0.92\%$, the Fermi energy is located very close to the bottom of the conduction band, suggesting that this value of the concentration is only slightly higher than the critical concentration of IMT, $n_{\text{crit}}$, predicted for Te$_{Si}$-hyperdoped Si. From our first-principles calculation data and considering the ideal case in which only one type of defect is present in hyperdoped Si, we can argue that the IMT for isolated Te$_{Si}$ system occurs at a lower Te concentration than that for Te$_{Si}$-Te$_{Si}$ dimer. In particular, by the comparison between the electronic states obtained by first-principles data and the experimental conductivity presented in Sec. III B, within the approximations used, our first-principles results for Te$_{Si}$-Te$_{Si}$ dimer are in agreement with experimental data qualitatively, thus suggesting that very probably the Te$_{Si}$-Te$_{Si}$ plays a fundamental role as the driving force of IMT.

B. Temperature dependence of the conductivity

It is known that the real difference between insulators and metals is revealed only at zero temperature. The metallic state is defined by exhibiting finite conductivity as the temperature ($T$) approaches zero, whereas insulators exhibit vanishing conductivity as $T$ approaches zero. The temperature-dependent conductivity is shown in Fig. 4(a). The sample with the lowest Te concentration (Te-0.25%) clearly tends towards vanishing conductivity; the same is concluded for Te-0.50%, although measurements at lower temperature would be desirable to make it clearer. Samples with the highest Te concentrations (Te-2.0% and Te-2.5%) exhibit a much higher conductivity which is also insensitive to temperature down to 2 K. Note that their conductivities are comparable to that of shallow-impurity-doped Si with just-metallic concentrations [5] and higher than those of metallic Si doped with S and Se [13,14]. Therefore, these two samples are metallic, whereas samples...
Te-0.50% and Te-0.50% are insulating. The samples Te-1.0% and Te-1.5% lie near the critical regime of IMT which will be analyzed further in the following.

Figure 4(b) displays a rigorous experimental evidence of an IMT in the PLM-treated Te-hyperdoped Si samples, which exhibit peak Te concentrations (N) from $1.25 \times 10^{20}$ cm$^{-3}$ to $1.25 \times 10^{21}$ cm$^{-3}$ and carrier concentration (n) from $2.0 \times 10^{19}$ to $8.3 \times 10^{20}$ cm$^{-3}$ at 300 K. We compare the carrier concentrations measured at 2 and 300 K, which are calculated by taking an effective thickness of 120 nm. For sample Te-0.25% and sample Te-0.50%, the carrier concentration at 2 K is substantially lower than that at 300 K, a clear evidence for thermal excited states as the temperature decreases. However, samples with Te peak concentration higher than $5.7 \times 10^{20}$ cm$^{-3}$ (Te-1.0%) exhibit temperature-independent carrier concentrations. Here, sample Te-1.0% ($n = 1.7 \times 10^{20}$ cm$^{-3}$) seems to be right at the border, suggesting that Te-1.5% is already metallic.

The conductivity in the metallic phase can be modeled to the form [35]

$$\sigma(T) = \sigma_0 + mT^s$$  

where $\sigma_0$ represents the zero-Kelvin conductivity, $m$ is a constant, and the temperature exponent $s$ is related to the scattering mechanism in the metallic phase. Electron-electron interactions in disordered systems lead to the lowest-order correction $mT^{1/2}$ to $\sigma_0$ [5,36], therefore we fixed the temperature exponent $s$ as 1/2 in the modeling. As Mott originally determined, the IMT in the group-IV semiconductors can be estimated as

$$n_\text{crit}^{1/3}a_H = 0.25,$$  

where $a_H$ is the effective Bohr radius of the donor electrons [1,33]:

$$a_H = \frac{e^2}{8\pi \varepsilon_0 \varepsilon_r E},$$

where $E$ is the binding (or activation) energy of the localized states, and $\varepsilon_0$ and $\varepsilon_r$ are the permittivity of free space and the high-frequency dielectric constant, respectively. Thus, by taking into account the binding energy as 199 meV [31,34], the isotropic Bohr radius is calculated as 3.1 Å and the critical carrier concentration of Te-hyperdoped Si is approximately $n_\text{crit} = 5.24 \times 10^{20}$ cm$^{-3}$. However, in the Mott criterion, the $a_H$ of an isolated center is defined as an appropriate radius associated with a realistic wave function for the localized state in the low-electron-density regime. In this case, the broadening of the electron wave function increases with the doping concentration. Therefore, the critical carrier concentration obtained from the experimental data (between $1.7 \times 10^{20}$ cm$^{-3}$ and $4.4 \times 10^{20}$ cm$^{-3}$; see the conclusion from Fig. 4) is actually lower than that from the value computed by the Mott criterion.
proposed, a minimum metallic conductivity \( \sigma_M \) at \( T = 0 \) K can be defined as \([37]\)

\[
\sigma_M = \frac{C e^2}{\hbar d_c},
\]

where the numerical coefficient \( C \approx 0.12 \) is for \( n \)-Si \([38]\) and \( d_c \) is the average spacing between impurity atoms at the critical concentration \( n_c \). Here \( \sigma_M \) with the value of \( 247 (\Omega \text{ cm})^{-1} \) is obtained by using \( d_c = (n_c)^{-1/3} \). Figure 5(a) shows the plot \( \sigma \) (conductivity) vs \( T^{-1/2} \) for samples with high Te concentration \( N \). The relationship \( \sigma(T) = \sigma_0 + mT^{-1/2} \) is approximately obeyed between 2 and 25 K, furthermore, the overall \( T \) dependence for the samples with different Te concentrations \( N \) makes the extrapolation to \( T = 0 \) rather unambiguous. Samples with high Te concentrations exhibit \( \sigma_0 \geq \sigma_M \), indicative of the metallic phase and consistent with the Mott picture. Figure 5(b) displays the extrapolated \( \sigma_0 \) as a function of carrier concentration \( n \). The critical behaviour is highly suggested by the sharpness of the transition, which is remarkable and is qualitatively close to the discontinuity predicted by Mott \([37]\). The fitting of the Eq. (3) yields \( \sigma_0(n, 0) = \sigma_0 \left( \frac{n}{n_c} - 1 \right)^\mu \) with \( \sigma_0 = 985 (\Omega \text{ cm})^{-1} \) (almost four times of \( \sigma_M \)), \( n_c = 1.54 \times 10^{20} \text{ cm}^{-3} \) and the critical conductivity exponent \( \mu = 0.48 \pm 0.07 \).

Figure 5(c) shows temperature correction \( m \) [extrapolated from Fig. 5(a)] plotted against carrier concentration \( n \) for samples with carrier concentration in the range of \( 1.1 < n/n_c < 5.4 \). As being well established, two classical models were proposed for the explanation of \( m \) (the correction to \( \sigma_0 \)): the scaling theory of localization \([2,39]\) and the Coulomb interaction with electron-electron scattering \([40–42]\). The latter is valid for \( k_F l \gg 1 \) \([5]\). Here \( k_F \) is the Fermi wave vector given by \([43]\)

\[
k_F = \left( \frac{3\pi^2}{8} n \right)^{1/3},
\]

where \( g = 6 \) is the number of equivalent minima in the conduction band of Si; \( l \) is the mean free path, which scales as

\[
l = \frac{3\pi^2}{4} \frac{\hbar}{e^2} \frac{\sigma_0}{k_F^2}.
\]

As shown in Fig. 5(c), a positive value of \( m \) term is produced for insulating samples. This would be consistent with the scaling theory of localization extended to include inelastic scattering but neglecting Coulomb interactions \([2,39]\). Also, here \( k_F l \) is no longer significantly greater than \( 1 \). \( m \) does not significantly change in the critical transition regime \( (n/n_c \approx 1.1 - 2.9) \), while towards larger \( n \), \( m \) changes the sign from positive to negative for samples with \( n/n_c > 2.9 \). This is in agreement with the reported work (P or As doped Si) \([5,44,45]\), resulting from the Coulomb interactions with electron-electron scattering in the presence of random impurities. However, one has to note that the lowest measurement temperature is \( 2 \) K in our case, which is much higher than some mK used in other cases. The lack of the data at mK temperatures and the detailed variation of Te concentration around \( 1.0\% \) could result in errors in both \( n_c \) and \( m \).

![FIG. 5. Analysis of temperature-dependent transport properties for metallic samples. (a) Electrical conductivity \( \sigma \) vs \( T^{-1/2} \) for Te-hyperdoped Si samples with high Te concentration \( N \). (b) Extrapolated conductivity \( \sigma_0 \) as a function of carrier concentration \( n \). The \( \sigma_0 \) data were fitted by \( \sigma_0(n, 0) = \sigma_0 \left( \frac{n}{n_c} - 1 \right)^\mu \) with \( \mu = 0.48 \pm 0.07 \). \( n_c = 1.54 \times 10^{20} \text{ cm}^{-3} \). (c) Coefficient \( m \) of the \( T \) dependence of \( \sigma \) vs carrier concentration.

2. Insulating samples

The electrical conductance in the insulating phase at low temperature can be achieved by hopping through the localized
deep levels [46]. The conductivity scales as
\[
\sigma(T) = \sigma_0 \exp \left[ -\left( \frac{T_p}{T} \right)^p \right].
\] (7)

The prefactor $\sigma_0$ and the characteristic temperature $T_p$ are related to material parameters by different relationships for each value of $p$. The exponent $p$ depends on the temperature and the shape of the density of the states (DOS) near the Fermi level. In detail, $p = 1/4$, $1/3$, $1/2$, or 1 corresponds to Mott-law variable-range hopping for 3D and 2D systems, the Efros-Shklovskii-type variable-range hopping (a Coulomb gap in the DOS), and the nearest-neighbor hopping, respectively [46]. To explicitly describe the temperature dependence of the conductivity and determine the value of $p$, Zabrodskii and Zinovevawas [47] introduced the reduced activation energy $W$ defined as
\[
W(T) = \frac{d \ln \sigma}{dT} = \frac{T}{\sigma} \frac{d\sigma}{dT}.
\] (8)

which enables us to determine which charge transport mechanism is mostly dominant among metallic, insulating, and the boundary of the IMT. Therefore, for the materials in the insulating phase, inserting Eq. (7) into Eq. (8) gives
\[
W(T) = p \left( \frac{T_p}{T} \right)^p.
\] (9)

As shown in Fig. 6(a), the data are replotted as $W(T)$ versus temperature on a log-log scale. For conductivity described as in Eq. (9), the slope of $\log W$ versus $\log T$ yields the value of $p = 0.45 \pm 0.04$ in the temperature range of $T < 50$ K. By this analysis, the values are very close to $p = 1/2$, which corresponds to the conduction of the Efros-Shklovskii-type variable-range hopping (ES law) [46]. This is the case where the impurity levels are deep enough and in turn the Coulomb gap is fairly large and has a certain vicinity of the Fermi level. The experimental results here indicate that the Coulomb gap is symmetric with respect to the Fermi level in the IB. This is consistent with the DFT calculation results considering the fact that $T_S$ and $T_S$-Te coexist in sample Te-0.25% [24].

Figure 6(b) displays the conductivity of semi-insulating samples as the function of $T^{-1/2}$. As the doping concentration approaches $n_c$, a sharp increase of conductivity is observed in the samples with small difference of impurity concentration. The fitting of variable-range hopping conductivity of insulating samples is presented in Fig. 6(b) as the solid lines. The fitting parameter $p = 1/2$ provides a reasonable fit with an average relative mean square error of 1.2% and the fitting range is restricted to $T < 50$ K. According to the law of Efros and Shklovskii [2], the characteristic parameter $T_p$ [in Eq. (7)] is related to fundamental material properties:
\[
T_p = \frac{C e^2}{4 \pi \varepsilon_0 \varepsilon k_B \xi},
\] (10)

where $e$ is the electron charge, $\varepsilon$ is the material permittivity, $k_B$ is the Boltzmann constant, $\xi$ is the electron correlation length, and $C = 2.8$ is a numerical coefficient [2,48,49]. $T_p$ can be obtained from the data fitting using Eq. (7): $T_p = 548$ K (47 meV) for sample Te-0.25% and $T_p = 180$ K (16 meV) for sample Te-0.50%. Knowing $T_p$, the material permittivity [50], and using Eq. (10), the electron correlation length $\xi$ can be computed. The electron correlation length $\xi$ increases from 7 nm in sample Te-0.25% to 22 nm in sample Te-0.50%. $\xi$ increases as the Te doping concentration increases. This indicates that the dopant concentration approaches the critical transition concentration of the IMT [49,50]. This is also corroborated in our DFT calculations.

V. CONCLUSION

In conclusion, we have investigated the transport properties of Te-hyperdoped Si samples prepared by ion implantation followed by nanosecond pulsed-laser melting. An insulator-to-metal transition driven by increasing Te concentration is confirmed and illustrates an agreement with the DFT computational results as well as with Mott’s theoretical picture. By performing the physical modeling for the temperature-dependent transport data, we have demonstrated that at sufficiently low temperatures the metallic samples show a power-law dependence whereas the insulating samples reveal
a variable-range-hopping-type conduction with a Coulomb gap at the Fermi level. These experimental findings have allowed us to identify the critical behavior near the IMT in Te-hyperdoped Si and have confirmed the effect of disorder and electron-electron interactions induced by Te dopants on the electron wave functions.

ACKNOWLEDGMENTS

Authors acknowledge the ion implantation group at HZDR for performing the Te implantations. Additionally, support by the Structural Characterization Facilities at Ion Beam Center (IBC) is gratefully acknowledged. This work was funded by the Helmholtz-Gemeinschaft Deutscher Forschungszentren (Grant No. HGF-VH-NG-713). The authors thank T. Ma and P. Shi for MATLAB introduction. M.W. acknowledges financial support by the Chinese Scholarship Council (File No. 201506240060). A.D. acknowledges CINECA for computational resources allocated under the ISCRA initiative (IMeCS project) and thanks R. Colnaghi for technical support on computer hardware.

[1] N. F. Mott, Metal-insulator transition, Rev. Mod. Phys. 40, 677 (1968).
[2] I. Shlimak, Is Hopping a Science? Selected Topics of Hopping Conductivity (World Scientific, Singapore, 2015).
[3] I. Shlimak, M. Kaveh, R. Ussyshkin, V. Ginodman, and L. Resnick, Unification of the metal-insulator transitions driven by the impurity concentration and by the magnetic field in arsenic-doped germanium, Phys. Rev. B 55, 1303 (1997).
[4] C. P. S. Waffenschmidt and H. V. Löhmeysen, Critical Behavior of the Conductivity of SiP at the Metal-Insulator Transition under Uniaxial Stress, Phys. Rev. Lett. 83, 3005 (1999).
[5] T. Rosenbaum, R. Milligan, M. Paalanen, G. Thomas, R. Bhatt, and W. Lin, Metal-insulator transition in a doped semiconductor, Phys. Rev. B 27, 7509 (1983).
[6] M. Paalanen, T. Rosenbaum, G. Thomas, and R. Bhatt, Stress Tuning of the Metal-Insulator Transition at Millikelvin Temperatures, Phys. Rev. Lett. 48, 1284 (1982).
[7] N. Mott, On the transition to metallic conduction in semiconductors, Can. J. Phys. 34, 1356 (1956).
[8] T. Castner, N. Lee, G. Cieloszyk, and G. Salinger, Dielectric Anomaly and the Metal-Insulator Transition in n-Type Silicon, Phys. Rev. Lett. 34, 1627 (1975).
[9] P. Newman and D. Holcomb, Metal-insulator transition in Si: As, Phys. Rev. B 28, 638 (1983).
[10] R. Hull, Properties of Crystalline Silicon (INSPEC, London, 1999).
[11] F. A. Trumbore, Solid solubilities of impurity elements in germanium and silicon, Bell Labs Tech. J. 39, 205 (1960).
[12] M. N. Alexander and D. F. Holcomb, Semiconductor-to-metal transition in n-type group IV semiconductors, Rev. Mod. Phys. 40, 815 (1968).
[13] M. T. Winkler, D. Recht, M. J. Sher, A. J. Said, E. Mazur, and M. J. Aziz, Insulator-to-Metal Transition in Sulfur-Doped Silicon, Phys. Rev. Lett. 106, 178701 (2011).
[14] E. Ertekin, M. T. Winkler, D. Recht, A. J. Said, M. J. Aziz, T. Buonassisi, and J. C. Grossman, Insulator-to-Metal Transition in Selenium-Hyperdoped Silicon: Observation and Origin, Phys. Rev. Lett. 108, 026401 (2012).
[15] Z. Y. Zhao and P. Z. Yang, Insight into insulator-to-metal transition of sulfur-doped silicon by DFT calculations, Phys. Chem. Chem. Phys. 16, 17499 (2014).
[16] F. Liu, S. Prucnal, Y. Berenécné, Z. Zhang, Y. Yuan, Y. Liu, R. Heller, R. Böttger, L. Rebohle, W. Skorupa, M. Helm, and S. Zhou, Realizing the insulator-to-metal transition in Se-hyperdoped Si via non-equilibrium material processing, J. Phys. D 50, 415102 (2017).
[17] M. Wang, Y. Berenécné, E. Garcia-Hemme, S. Prucnal, R. Hübner, Y. Yuan, C. Xu, L. Rebohle, R. Böttger, and R. Heller, Extended Infrared Photoresponse in Te-Hyperdoped Si at Room Temperature, Phys. Rev. Appl. 10, 024054 (2018).
[18] S. Hu, P. Han, P. Liang, Y. Xing, and S. Lou, Metallic conduction behavior in selenium-hyperdoped silicon, Mater. Sci. Semicond. Process. 17, 134 (2014).
[19] P. Giannozzi, S. Baroni, N. Bonini, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, G. L. Chiarotti, M. Cococcioni, I. Dabo et al., QUANTUM ESPRESSO: A modular and open-source software project for quantum simulations of materials, J. Phys.: Condens. Matter 21, 395502 (2009).
[20] A. M. Rappe, K. M. Rabe, E. Kaxiras, and J. D. Joannopoulos, Optimized pseudopotentials, Phys. Rev. B 41, 1227 (1990).
[21] D. Vanderbilt, Optimally smooth norm-conserving pseudopotentials, Phys. Rev. B 32, 8412 (1985).
[22] D. Vanderbilt, Soft self-consistent pseudopotentials in a generalized eigenvalue formalism, Phys. Rev. B 41, 7892(R) (1990).
[23] L. Kleinmann and D. M. Bylander, Efﬁcacious Form for Model Pseudopotentials, Phys. Rev. Lett. 48, 1425 (1982).
[24] M. Wang, A. Debernardi, Y. Berencéné, R. Heller, C. Xu, Y. Yuan, Y. Xie, R. Böttger, L. Rebohle, W. Skorupa, M. Helm, S. Prucnal, and S. Zhou, Breaking the Doping Limit in Silicon by Deep Impurities, Phys. Rev. Appl. 11, 054039 (2019).
[25] J. F. Ziegler, SRIM-2003, Nucl. Instrum. Methods Phys. Res. B 219, 1027 (2004).
[26] F. Spaepen, D. Turnbull, J. Poate, and J. Mayer, Laser Annealing of Semiconductors (Academic Press, New York, 1982).
[27] M. Mayer, SIMNRA user’s guide, Report No. IPP 9/113, Max-Planck-Institut für Plasmaphysik (Garching, Germany, 1997).
[28] M. Mayer, SIMNRA, a simulation program for the analysis of NRA, RBS and ERDA, edited by J. L. Duggan and I. L. Morgan, AIP Conf. Proc. No. 475 (AIP, Melville, NY, 1999), p. 541.
[29] L. Van der Pauw, A method of measuring the resistivity and hall coefficient on lamellae of arbitrary shape, Philips Tech. Rev. 20, 320 (1958).
[30] J. W. Mayer, Gold contacts to semiconductor devices, Gold Bull. 17, 18 (1984).
[31] R. Schaub, G. Pensl, M. Schulz, and C. Holm, Donor states in tellurium-doped silicon, Appl. Phys. A 34, 215 (1984).
[32] E. Janzén, R. Stedman, G. Grossmann, and H. G. Grimmmeiss, High-resolution studies of sulfur- and selenium-related donor centers in silicon, Phys. Rev. B 29, 1907 (1984).
[33] N. F. Mott, Metal-insulator transitions, Contemp. Phys. 14, 401 (1973).

[34] K. Sáñchez, I. Aguilera, P. Palacios, and P. Wahnón, Formation of a reliable intermediate band in Si heavily coimplanted with chalcogens (S, Se, Te) and group III elements (B, Al), Phys. Rev. B 82, 165201 (2010).

[35] P. A. Lee and T. V. Ramakrishnan, Disordered electronic systems, Rev. Mod. Phys. 57, 287 (1985).

[36] B. L. Altshuler and A. G. Aronov, Damping of one-electron excitations in metals, JETP Lett. 30, 482 (1979).

[37] N. Mott, The minimum metallic conductivity in three dimensions, Philos. Mag. B 44, 265 (1981).

[38] I. Shlimak and M. Kaveh, State of Mott minimal metallic conductivity in a scaling approach to the metal-insulator transition in doped semiconductors, Phys. Rev. B 58, 15333 (1998).

[39] E. Abrahams, P. Anderson, D. Licciardello, and T. Ramakrishnan, Scaling Theory of Localization: Absence of Quantum Diffusion in Two Dimensions, Phys. Rev. Lett. 42, 673 (1979).

[40] B. Altshuler and A. Aronov, Fermi-liquid theory of the electron-electron interaction effects in disordered metals, Solid State Commun. 46, 429 (1983).

[41] B. L. Altshuler and A. G. Aronov, in Electron-Electron Interactions in Disordered Systems, edited by M. Pollak and A. L. Efros (North-Holland, Amsterdam, 1985).

[42] B. Kramer and A. MacKinnon, Localization: Theory and experiment, Rep. Prog. Phys. 56, 1469 (1993).

[43] C. Kittel, Introduction to Solid State Physics (Wiley, New York, 1976), Vol. 8.

[44] W. N. Shafarman, D. W. Koon, and T. G. Castner, Dc conductivity of arsenic-doped silicon near the metal-insulator transition, Phys. Rev. B 40, 1216 (1989).

[45] H. Stupp, M. Hornung, M. Lakner, O. Madel, and H. Lohneysen, Possible Solution of the Conductivity Exponent Puzzle for the Metal-Insulator Transition in Heavily Doped Uncompensated Semiconductors, Phys. Rev. Lett. 71, 2634 (1993).

[46] B. I. Shklovskii and A. L. Efros, Electronic Properties of Doped Semiconductors (Springer-Verlag, Berlin, 1984).

[47] A. G. Zabrodskii and K. N. Zinoveva, Critical behavior of N-Ge parameters in the region of compensation-induced Anderson transition, Zh. Eksp. Teor. Fiz. 86, 727 (1984) [Sov. Phys. JETP 37, 727 (1983)].

[48] S. Baranovskii, A. Efros, B. Gelmont, and B. Shklovskii, Coulomb gap in disordered systems: Computer simulation, J. Phys. C: Solid State Phys. 12, 1023 (1979).

[49] D. A. Neamen, Semiconductor Physics and Devices: Basic Principles (Irwin, Boston, 1997).

[50] A. Zabrodskii, The coulomb gap: The view of an experimenter, Philos. Mag. B 81, 1131 (2001).