Search for magnetically-induced signatures in the arrival directions of ultra-high-energy cosmic rays measured at the Pierre Auger Observatory

A. Aab, P. Abreu, M. Aglietta, J.M. Albury, I. Allekotte, A. Almela, J. Alvarez Castillo, J. Alvarez-Muñiz, R. Alves Batista, G.A. Anastasi, L. Anchordoqui, B. Andrade, S. Andringa, C. Aramo, P.R. Araújo Ferreira, H. Asorey, P. Assis, G. Avila, A.M. Badescu, A. Bakalova, A. Balaceanu, F. Barbato, R.J. Barreira Luz, K.H. Becker, J.A. Bellido, C. Berat, M.E. Bertaina, X. Bertou, P.L. Biermann, T. Bister, J. Biteau, A. Blanco, J. Blazek, C. BLEVE, M. Buscemi, K.S. Caballero-Mora, L. Caccianiga, L. Calcagni, A. Cancio, F. Canfora, I. Caracas, J.M. Carceller, R. Caruso, A. Castellina, G. Cataldi, L. Cazon, M. Cerda, J.A. Chinellato, K. Choi, J. Chudoba, L. Chytka, R.W. Clay, A.C. Cobos Cerutti, R. Colalillo, A. Coleman, M.R. Coluccia, R. Conceição, A. Condorelli, G. Consolati, F. Contreras, F. Convenga, C.E. Covault, S. Dasso, K. Daumiller, B.R. Dawson, J.A. Day, R.M. de Almeida, J. de Jesús, S.J. de Jong, G. De Mauro, J.R.T. de Mello Neto, I. De Mitri, J. de Oliveira, D. de Oliveira Franco, V. de Souza, J. Debatin, M. del Río, O. Deligny, N. Dhital, A. Di Matteo, M.L. Díaz Castro, C. Dobrigkeit, J.C. D’Olivo, Q. Dorosti, R.C. dos Anjos,
M.T. Dova, J. Ebr, R. Engel, I. Epicoco, M. Erdmann, C.O. Escobar, A. Etchegoyen, H. Falcke, J. Farmer, G. Farrar, A.C. Fauth, N. Fazzini, F. Feldbusch, F. Fenu, B. Fick, J.M. Figueira, A. Filipčič, T. Fodran, M.M. Freire, H. Falcke, A. Fuster, C. Galea, C. Galelli, B. García, A.L. Garcia Vegas, H. Gemmeke, F. Gesualdi, A. Gherghel-Lascu, P.L. Ghia, M. Giammarchi, M. Giller, J. Glombitza, G. Golup, M. Gómez Berisso, P.F. Gómez Vitale, J.P. Gongora, N. González, I. Goos, D. Góra, A. Gorgi, M. Gottowik, T.D. Grubb, F. Guarino, G.P. Guedes, E. Guido, S. Hahn, R. Halliday, M.R. Hampel, P. Hansen, D. Harari, V.M. Harvey, A. Haungs, T. Hebbeker, D. Heck, G.C. Hill, C. Hojvat, J.R. Hörandel, P. Horvath, M. Hrabovský, T. Huege, J. Hulsman, A. Insolia, P.G. Isar, J.A. Johnsen, J. Jurysek, A. Kääpä, K.H. Kampert, B. Keilhauer, J. Kemp, H.O. Klages, M. Kleifges, J. Kleinfeller, M. Köpke, G. Kukec Mezek, T. Lago, D. LaHurd, R.G. Lang, M.A. Leigui de Oliveira, V. Lenok, A. Letessier-Selvon, I. Lhenry-Yvon, D. Lo Presti, L. Lopes, R. López, R. Lorek, Q. Luce, A. Lucero, A. Machado Payeras, M. Malacari, G. Mancarella, D. Mandat, B.C. Manning, J. Manshanden, P. Mantsch, S. Marafico, A.G. Mariazzi, I.C. Mariš, G. Marsella, D. Martello, H. Martinez, O. Martínez Bravo, M. Mastrodicasa, H.J. Mathes, J. Matthews, G. Matthiae, E. Mayotte, P.O. Mazur, G. Medina-Tanco, D. Melo, A. Menshikov, K.-D. Merenda, S. Michal, M.I. Micheletti, L. Miramonti, D. Mockler, S. Mollerach, F. Montanet, C. Morello, M. Mostafá, A.L. Müller, M.A. Muller, K. Mulrey, R. Mussa, M. Muzio, W.M. Namasaka, L. Nellen, M. Niculescu-Oglinzanu, M. Niechciol, D. Nitz, D. Nosek, V. Novotny, L. Nožka, A Nucita, L.A. Núñez, M. Palatka, J. Pallotta, M.P. Panetta, P. Papenbreer, G. Parente, A. Parra, M. Pech, F. Pedreira, J. Pekala, R. Pelayo, J. Peña-Rodriguez,
J. Perez Armand, 19 M. Perlin, 8,37 L. Perrone, 52,45 C. Peters, 39
S. Petrera, 42,43 T. Pierog, 37 M. Pimenta, 67 V. Pirronello, 54,44
M. Platino, 8 B. Pont, 75 M. Pothast, 77,75 P. Privitera, 87
M. Prouza, 30 A. Puyleart, 84 S. Querchfeld, 35 J. Rautenberg, 35
D. Ravignani, 8 M. Reininghaus, 37,8 J. Ridky, 30 F. Riehn, 87
M. Risse, 41 P. Ristori, 2 V. Rizi, 53,43 W. Rodrigues de Carvalho, 19
J. Rodriguez Rojo, 9 M.J. Roncoroni, 8 M. Roth, 37 E. Roulet, 1
A.C. Rovero, 5 P. Ruehl, 41 S.J. Saffi, 12 A. Saftoiu, 68
F. Salamida, 53,43 H. Salazar, 59 G. Salina, 48 J.D. Sanabria
Gomez, 28 F. Sánchez, 8 E.M. Santos, 19 E. Santos, 30 F. Sarazin, 81
R. Sarmento, 67 C. Sarmento-Cano, 8 R. Sato, 9 P. Savina, 52,45,32
C. Schäfer, 37 V. Scherini, 45 H. Schieler, 37 M. Schimassek, 36,8
M. Schimp, 35 F. Schlüter, 37,8 D. Schmidt, 36 O. Scholtens, 76,14
P. Schovánek, 30 F.G. Schröder, 88,37 S. Schröder, 35 J.S. Sciutto, 4
M. Scornavacche, 8,37 R.C. Shellard, 15 G. Sigl, 40 G. Silli, 8,37
O. Sima, 68,8 R. Šmída, 87 P. Sommer, 86 J.F. Soriano, 82
J. Souchard, 34 R. Squartini, 9 M. Stadelmaier, 37,8 D. Stanca, 68
S. Stanič, 71 J. Stasielak, 64 P. Stassi, 34 A. Streich, 36,8
M. Suárez-Durán, 28 T. Sudholz, 12 T. Suomijärvi, 32
A.D. Supanitsky, 8 J. Šupík, 31 Z. Szadkowski, 66 A. Taboada, 36
A. Tapia, 27 C. Timmermans, 77,75 P. Tobiska, 30 C.J. Todero
Peixoto, 17 B. Tomé, 67 G. Torralba Elipe, 74 A. Travaini, 9
P. Travnichek, 30 C. Trimarelli, 53,43 M. Trini, 71 M. Tueros, 4
R. Ulrich, 37 M. Unger, 37 M. Urban, 39 L. Vaclavek, 31 M. Vacula, 31
J.F. Valdés Galicia, 63 I. Valiño, 42,43 L. Valore, 56,47 A. van Vliet, 75
E. Varela, 59 B. Vargas Cardenas, 63 A. Vásquez-Ramírez, 28
D. Veberić, 37 C. Ventura, 25 I.D. Vergara Quispe, 4 V. Verzi, 48
J. Vicha, 30 L. Villaseñor, 59 J. Vink, 79 S. Vorobiov, 71
H. Wahlberg, 4 A.A. Watson, a M. Weber, 38 A. Weindl, 37
L. Wiencke, 81 H. Wilczyński, 64 T. Winchen, 14 M. Wirtz, 39
D. Wittkowski, 35 B. Wundheiler, 8 A. Yushkov, 30
O. Zapparrata, 13 E. Zas, 74 D. Zavrtanik, 71,72 M. Zavrtanik, 72,71
L. Zehrer, 71 A. Zepeda, 60 M. Ziolkowski, 41 and F. Zuccarello 54,44

1Centro Atómico Bariloche and Instituto Balseiro (CNEA-UNCuyo-CONICET), San Carlos
de Bariloche, Argentina
2Centro de Investigaciones en Láseres y Aplicaciones, CITEDEF and CONICET, Villa
Martelli, Argentina
3Departamento de Física and Departamento de Ciencias de la Atmósfera y los Océanos,
FCEyN, Universidad de Buenos Aires and CONICET, Buenos Aires, Argentina
4IFLP, Universidad Nacional de La Plata and CONICET, La Plata, Argentina
Instituto de Astronomía y Física del Espacio (IAFE, CONICET-UBA), Buenos Aires, Argentina
6 Instituto de Física de Rosario (IFIR) – CONICET/U.N.R. and Facultad de Ciencias Bioquímicas y Farmacéuticas U.N.R., Rosario, Argentina
7 Instituto de Tecnologías en Detección y Astroparticulas (CNEA, CONICET, UNSAM), and Universidad Tecnológica Nacional – Facultad Regional Mendoza (CONICET/CNEA), Mendoza, Argentina
8 Instituto de Tecnologías en Detección y Astroparticulas (CNEA, CONICET, UNSAM), Buenos Aires, Argentina
9 Observatorio Pierre Auger, Malargüe, Argentina
10 Observatorio Pierre Auger and Comisión Nacional de Energía Atómica, Malargüe, Argentina
11 Universidad Tecnológica Nacional – Facultad Regional Buenos Aires, Buenos Aires, Argentina
12 University of Adelaide, Adelaide, S.A., Australia
13 Université Libre de Bruxelles (ULB), Brussels, Belgium
14 Vrije Universiteit Brussels, Brussels, Belgium
15 Centro Brasileiro de Pesquisas Físicas, Rio de Janeiro, RJ, Brazil
16 Centro Federal de Educación Tecnológica Celso Suckow da Fonseca, Nova Friburgo, Brazil
17 Universidade de São Paulo, Escola de Engenharia de Lorena, Lorena, SP, Brazil
18 Universidade de São Paulo, Instituto de Física de São Carlos, São Carlos, SP, Brazil
19 Universidade de São Paulo, Instituto de Física, São Paulo, SP, Brazil
20 Universidade Estadual de Campinas, IFGW, Campinas, SP, Brazil
21 Universidade Estadual de Feira de Santana, Feira de Santana, Brazil
22 Universidade Federal do ABC, Santo André, SP, Brazil
23 Universidade Federal do Paraná, Setor Palotina, Palotina, Brazil
24 Universidade Federal do Rio de Janeiro, Instituto de Física, Rio de Janeiro, RJ, Brazil
25 Universidade Federal do Rio de Janeiro (UFRJ), Observatório do Valongo, Rio de Janeiro, RJ, Brazil
26 Universidade Federal Fluminense, EEIMVR, Volta Redonda, RJ, Brazil
27 Universidad de Medellín, Medellín, Colombia
28 Universidad Industrial de Santander, Bucaramanga, Colombia
29 Charles University, Faculty of Mathematics and Physics, Institute of Particle and Nuclear Physics, Prague, Czech Republic
30 Institute of Physics of the Czech Academy of Sciences, Prague, Czech Republic
31 Palacky University, RCPTM, Olomouc, Czech Republic
32 Université Paris-Saclay, CNRS/IN2P3, IJCLab, Orsay, France, France
33 Laboratoire de Physique Nucléaire et de Hautes Energies (LPNHE), Universités Paris 6 et Paris 7, CNRS-IN2P3, Paris, France
34 Univ. Grenoble Alpes, CNRS, Grenoble Institute of Engineering Univ. Grenoble Alpes, LPSC-IN2P3, 38000 Grenoble, France, France
35 Bergische Universität Wuppertal, Department of Physics, Wuppertal, Germany
36 Karlsruhe Institute of Technology, Institute for Experimental Particle Physics (ETP), Karlsruhe, Germany
37 Karlsruhe Institute of Technology, Institut für Kernphysik, Karlsruhe, Germany
Abstract. We search for signals of magnetically-induced effects in the arrival directions of ultra-high-energy cosmic rays detected at the Pierre Auger Observatory. We apply two different methods. One is a search for sets of events that show a correlation between their arrival direction and the inverse of their energy, which would be expected if they come from the same point-like source, they have the same electric charge and their deflection is relatively small and coherent. We refer to these sets of events as “multiplets”. The second method, called “thrust”, is a principal axis analysis aimed to detect the elongated patterns in a region of interest. We study the sensitivity of both methods using a benchmark simulation and we apply them to data in two different searches. The first search is done assuming as source candidates a list of nearby active galactic nuclei and starburst galaxies. The second is an all-sky blind search. We report the results and we find no statistically significant features. We discuss the compatibility of these results with the indications on the mass composition inferred from data of the Pierre Auger Observatory.
1 Introduction

The identification of the sources of ultra-high-energy cosmic rays (UHECRs) is one of the main unsolved challenges in astrophysics. Since UHECRs are charged particles, their path from their sources to Earth is modified by the extragalactic and Galactic magnetic fields they traverse, most notably by the latter. The knowledge of these intervening fields is still poor, despite the considerable experimental effort in the area (see e.g. [1–3] and references therein).

Another element that makes the magnetic deflections difficult to predict is the uncertain composition of UHECRs. This is due to the fact that measurements of the maximum of the shower development, which depends on the mass of the primary particle, have low statistics at the highest energies and its interpretation depends on the modelling of the hadronic interactions. The results from the Pierre Auger Observatory [4–6] indicate that the composition becomes heavier with increasing energy. However, measurements do not rule out a light nuclei fraction at the highest energies, which might originate in a few nearby sources, different from the average ones. In such a case, the search for magnetically-induced signatures in the arrival directions of UHECRs could help identify this type of sources. Several analysis techniques have been designed to capture this kind of effect, including indirect ways such as in [7]. In this work, we show the results of two different methods applied to perform this search in a direct way, which are referred to as “multiplets” and “thrust”.

Multiplets are defined as a set of events that show a correlation between their arrival direction and the inverse of their energy, which is expected if they come from the same source, they have the same electric charge and their deflections are small and remain coherent. The observation of multiplets could enable the accurate identification of the direction of the source
and could also provide a new means to probe the Galactic magnetic field by inferring the value
of its integrated component orthogonal to the trajectory of cosmic rays.

A search for multiplets was performed by the Pierre Auger Collaboration in [8]. In
that work, data up to 31st December 2010 were used, which amounted to a total exposure of
25,800 km$^2$ sr yr. The results obtained were not statistically significant. The largest multiplet
found above 20 EeV had 12 events and the probability that it would appear by chance in an
isotropic distribution of events was 6%. There were also two independent 10-plets and the
chance probability of having at least three multiplets with a multiplicity equal to or larger
than 10 was 20%. With the larger dataset used in this work, the number of events added
to these multiplets is not statistically significant when comparing it to the number of events
that would be added if the arrival directions were isotropic, with a $p$-value of 60.5%.

In the thrust method, an observable is built from a principal axis analysis in a localized
region of the sky, measuring the elongation of a pattern with respect to the center of the
region of interest (ROI). The thrust method was applied to data by the Pierre Auger Collabora-
tion in [9], with events detected up to 19th March 2013, amounting to a total exposure
of 32,800 km$^2$ sr yr. The measured distributions of the thrust observables with the centroid
corresponding to the highest energy cosmic rays did not reveal any local patterns in the arrival
directions of UHECRs.

In this work, we update these analyses with more statistics. The data set used, which
amounts to a total exposure of 101,900 km$^2$ sr yr, is described in Section 2. This is an
increase of a factor 4 with respect to [8] and a factor 3 with respect to [9]. The methods
used are discussed in detail in Section 3. Their expected sensitivity is shown in Section 5,
using a benchmark simulation described in Section 4. The methods are applied to a targeted
search on a selection of nearby active galactic nuclei (AGNs) and starburst galaxies (SBGs),
candidates to be sites of ultra-high-energy (UHE) acceleration, and the results are presented
in Section 6. Moreover, in Section 7, we apply the methods to an all-sky blind search. Finally,
in Section 8, we present our conclusions.

2 The Pierre Auger Observatory and the data set

The Pierre Auger Observatory [10, 11], located in Malargüe, Argentina (35.2° S, 69.5° W,
1400 m a.s.l.), consists of a large surface detector (SD) and an air-fluorescence detector (FD),
which are used to observe extensive air showers generated by UHECRs in a complementary
way. The SD is composed of an array of 1660 water-Cherenkov stations, arranged in an
equilateral triangular grid, spread over an area of 3000 km$^2$. It measures, with a duty cycle
of nearly 100%, the energy flow in the shower carried by electrons, photons and muons that
reach ground level. The FD, comprising 27 telescopes at four sites, overlooks the surface
array and observes, with a duty cycle close to 15%, the fluorescence light emitted by nitrogen
molecules excited by the particles produced as the air shower develops in the atmosphere.

In this study, we select data recorded with the surface detector between 1st January
2004 and 31st August 2018 with zenith angles $\theta \leq 80°$. The energy thresholds we use are
20 EeV and 40 EeV, which yield data sets of 6568 and 1119 events, respectively. The “vertical”
events ($\theta \leq 60°$) are required to have at least four active stations surrounding the one with
the highest signal, while the “inclined” events ($\theta > 60°$) are required to have at least five
active stations. For the vertical events, the reconstructed core must be inside an equilateral
or isosceles triangle of active stations. This ensures an accurate reconstruction of the shower
geometry and energy.
The arrival directions of these cosmic rays are determined from the relative arrival times of the shower front in the triggered stations. The angular resolution, defined as the radius around the true cosmic-ray direction that would contain 68% of the reconstructed shower directions, is better than 1° for the energies considered here [12, 13]. The energy estimate is obtained from the signals recorded by the SD stations [14, 15] and is calibrated using “hybrid” events (detected simultaneously by SD and FD) and taking advantage of the quasi-calorimetric energy determination obtained with the FD [16]. The statistical uncertainty in the energy determination is smaller than 9% for the energies considered and the systematic uncertainty on the absolute energy scale is 14% [16].

At energies above 4 EeV, the SD trigger is fully efficient, and the determination of the exposure is purely geometrical [17]. For the time period considered and for the applied energy and zenith angle selection, it amounts to 101,900 km² sr yr.

3 Methods

3.1 Multiplets

If the deflection is small, it is a good approximation [18] to consider that the relation between the arrival direction of the cosmic ray \( \vec{\Theta} \) and the actual source direction \( \vec{\Theta}_s \),

\[
\vec{\Theta} = \vec{\Theta}_s + \frac{Ze}{E} \int_0^L d\vec{\ell} \times \vec{B}(\vec{\ell}).
\]  

(3.1)

This equation can be simplified to yield the following linear relation with the inverse of the energy \( E \) of the cosmic ray:

\[
\vec{\Theta} \simeq \vec{\Theta}_s + \frac{\vec{D}(\vec{\Theta}_s)}{E}.
\]  

(3.2)

Here \( \vec{D} \) is the integral along the line of sight of the perpendicular component of the magnetic field \( \vec{B} \) times the charge \( Ze \) of the particle, and is approximated to a constant for a fixed source direction. The “deflection power” \( D \equiv |\vec{D}| \) will be given in units \( 1° \times 100 \) EeV.

To determine if a set of cosmic rays forms a multiplet, we first use a coordinate system \((x, y)\) in the tangent plane to the celestial sphere (centered on the average direction of the events). The system is then rotated to a system \((u, w)\) with an angle such that the covariance

\[
\text{Cov}(w, 1/E) = \frac{1}{N} \sum_{i=1}^{N} (w_i - \langle w \rangle)(1/E_i - \langle 1/E \rangle)
\]  

(3.3)

between the cosmic ray coordinates \( w_i \) and their inverse energy \( 1/E_i \) is zero and the covariance \( \text{Cov}(u, 1/E) \) is maximal. This angle is given by

\[
\alpha = \arctan \left( \frac{\text{Cov}(y, 1/E)}{\text{Cov}(x, 1/E)} \right). \]

(3.4)

The correlation between the coordinate \( u \) and \( 1/E \) is measured through the correlation coefficient

\[
C(u, 1/E) = \frac{\text{Cov}(u, 1/E)}{\sqrt{\text{Var}(u)\text{Var}(1/E)}}
\]  

(3.5)

where the variances are given by \( \text{Var}(x) = \langle (x - \langle x \rangle)^2 \rangle \).
The cuts applied to identify possible candidates among background chance alignments are: i) a minimum value for the correlation coefficient, $C(u, 1/E) > C_{\text{min}}$, and ii) a maximum value for the spread in the transverse direction of the multiplet, $\max(|w_i - \langle w \rangle|) < W_{\text{max}}$. In [8], the two parameters chosen were $C_{\text{min}} = 0.9$ and $W_{\text{max}} = 1.5^\circ$. They were adopted following a search for a compromise between maximizing the signal from a true source and minimizing the background arising from chance alignments. To do so, numerical simulations were performed with sets of protons from randomly-located extragalactic sources, which were propagated through a bisymmetric magnetic field with even symmetry and a simple random deflection with root mean square amplitude $1.5^\circ \times (20\text{EeV}/E)$ to simulate the turbulent field. In this work, we tested variations of these parameters using the more up-to-date simulation described in Section 4 and, as it is shown in Section 5.1, these values for the cuts still perform well. A third cut used here consists in searching for multiplets which extend up to $20^\circ$ in the sky and with energies above $40\text{EeV}$, so that the linear correlation of the deflection with $1/E$ is expected to be valid for “light” nuclei, such as emitted by proton and helium sources. We also test the sensitivity of the method making a search of events with energies between $20\text{EeV}$ and $40\text{EeV}$, where the linear approximation is still valid for proton sources.

3.2 Thrust ratio

Deviations from a clear correlation between the energy and the deflection angle can arise from large turbulent field components or from a mixed nuclear composition of the cosmic rays, as deflections scale also with the nuclear charges $Z_i$ of the particles. In this case, the thrust ratio, $T_2/T_3$, can still capture an elongation of the arising pattern in the arrival directions. The thrust observables $T_k$ ($k = 1, 2, 3$) are constructed by successively maximizing the values

$$T_k = \max_{\hat{n}_k} \left( \frac{\sum_i |\omega_i^{-1}\vec{p}_i \cdot \hat{n}_k|}{\sum_i |\omega_i^{-1}\vec{p}_i|} \right)$$

with respect to the axes $\hat{n}_k$ starting with $k = 1$. The sum iterates over all cosmic rays in the chosen region of interest (ROI), $\vec{p}_i$ is the arrival direction of particle $i$ weighted with its energy and $\omega_i$ is the exposure towards this direction. The principal axes $\hat{n}_k$ are perpendicular to each other ($\hat{n}_1 \perp \hat{n}_2 \perp \hat{n}_3$), thus, we obtain by construction for the thrust observables the relation $T_1 > T_2 > T_3$.

While the thrust axis $\hat{n}_1$ points radially to the local barycenter of the energy distribution within the ROI, the axes $\hat{n}_2$ and $\hat{n}_3$ form an orthonormal coordinate system tangential to the local spherical plane. In this system, a signal-like structure would be characterized by a strong collimation of arrival directions around the $\hat{n}_2$-axis, and therefore by a high thrust observable $T_2$. To be less affected by the radial cosmic-ray distribution within the ROI, we choose instead the thrust ratio $T_2/T_3$ as the relevant observable. Based on the simulations performed in Section 4, we choose for the ROI radius a value of $r_{\text{ROI}} = 0.3 \text{ rad} \ (\sim 17.2^\circ)$. A more detailed description of the procedure can be found in [9].

4 Target selection and benchmark simulation

In this Section, we describe the selection of astrophysical objects that have been discussed as promising candidates for UHE acceleration and which are used in a targeted search. We also give details of the simulation we used to evaluate the sensitivities of the two methods presented in the previous Section.
4.1 Target selection

In [19], we reported on a potentially interesting indication of anisotropy in the arrival direction of UHECRs given by an excess flux towards nearby galaxies. A maximum-likelihood ratio test was used with two free parameters, namely the fraction of events correlating with astrophysical objects and an angular scale characterizing the clustering of cosmic rays around extragalactic sources. Sky models of cosmic-ray density were constructed using two catalogs of source classes studied by Fermi-LAT [20, 21]: AGNs and SBGs. The relative luminosity of each source in UHECRs was assumed to be proportional to the $\gamma$-ray luminosity for the former and to the radio emission for the latter, for which the sample of detected sources in the $\gamma$-ray band remains scarce. When comparing both models to isotropic expectations, the most promising result was found with SBGs, with a statistical significance of 4.0$\sigma$. The result found with AGNs was also interesting, with a 2.7$\sigma$ deviation from isotropy. Results were updated in [24] and the statistical significances increased to 4.5$\sigma$ and 3.1$\sigma$ for the SBG and AGN models, respectively. The Telescope Array Collaboration tested these results with their observed events, but they found not to have enough statistics to confirm these results [25].

In this work, we include a search for magnetically-induced effects in the arrival directions of events close to potential candidates for UHE acceleration. For the multiplet search, we look for sets of events with a reconstructed source position within $3^\circ$ of these candidates. We also apply the thrust method centering the ROI in the position of the source candidates. We call these two analyses a “targeted search”.

To define the astrophysical objects that are chosen as source candidates, we used the catalogs from [20–23]. We divided the sample between AGNs and SBGs. Since we are interested in “light” UHECRs, we computed the flux at Earth as if these candidates would accelerate helium nuclei, accounting for the interactions from the sources to Earth. If with the methods used in this work we were able to detect such events, we would also be able to detect protons in the case they were also accelerated at these energies. In Figure 1, we show the flux contribution of these sources relative to the expected one from the brightest source in each sample, as a function of the distance to the object, taking also into account the non-uniform exposure on the celestial sphere of the Observatory. We simulated events with an energy above $40\text{EeV}$ and with an energy spectrum at the source being $dN/dE \propto E^{-2}$. We assume that these sources, different from the average ones, would contribute to a small fraction of the total measured flux. Hence, the spectrum assumed for these simulations would be compatible to the measured one. We present the results marginalized over the uncertainties on the measured energy and on the distance to the candidate.$^{1}$ We selected the candidates using a cut on the helium flux contribution of 1% relative to the object with the highest contribution (Cen A and NGC 4945 for the AGN and SBG catalogs, respectively). We also kept NGC 4631 since its contribution, 0.96%, is barely below the threshold. In Table 1, we list the ten source candidates that remain after this cut, which include three AGNs and seven SBGs.

---

$^{1}$The distance estimates employed in this work are based on [26] and [27], exploiting in particular the Tully-Fisher correlation or the tip of the red-giant branch. The typical uncertainty on high-quality distance estimators is estimated to 10% [29], which we adopt as the minimum uncertainty in the marginalization procedure. The largest variance in distance estimates over different methods is found for NGC 1068, for which redshift-based estimates go up to 19 Mpc [28]. Adopting the latter distance for NGC 1068 does not impact the selection of this source within the sample of candidate for emitters of elongated patterns of UHECR.
**Figure 1.** Relative flux with respect to the brightest object in each catalog (AGNs in blue empty circles and SBGs in red filled circles) as a function of the distance to the source candidate, accounting for the directional exposure of the Observatory and assuming that the accelerated and detected events are helium nuclei with an energy greater than 40 EeV. The results are marginalized over the uncertainties on the measured energy and on the distance to the candidate.

**Table 1.** Selection of astrophysical objects which could be candidates for UHE acceleration. Assuming that these candidates would accelerate helium nuclei, these objects are expected to contribute at least \(\sim 1\%\) with respect to the strongest source candidate in each catalog, accounting for propagation effects and the exposure of the Observatory.

| AGN source candidates | Target | Gal. longitude [°] | Gal. latitude [°] | Distance [Mpc] |
|-----------------------|--------|-------------------|------------------|---------------|
| Cen A                 | 309.5  | 19.4              |                  | 3.7 [26]      |
| M 87                  | 283.8  | 74.5              |                  | 17 [26]       |
| Fornax A              | 240.2  | −56.7             |                  | 17 [26]       |

| SBG source candidates | Target | Gal. longitude [°] | Gal. latitude [°] | Distance [Mpc] |
|-----------------------|--------|-------------------|------------------|---------------|
| NGC 253               | 97.4   | −88.0             |                  | 3.6 [26]      |
| NGC 4945              | 305.3  | 13.3              |                  | 3.7 [26]      |
| Circinus              | 311.3  | −3.8              |                  | 4.2 [27]      |
| M 83                  | 314.6  | 32.0              |                  | 4.7 [26]      |
| NGC 4631              | 142.8  | 84.2              |                  | 7.4 [26]      |
| NGC 1808              | 241.2  | −35.9             |                  | 9.1 [26]      |
| NGC 1068              | 172.1  | −51.9             |                  | 10 [27]       |

### 4.2 Benchmark simulation

To evaluate the performance of the methods presented in Section 3, we tested their sensitivity in a model where the UHECRs are accelerated in the source candidates presented in Section 4.1 (listed in Table 1) and then are propagated through a model of the intervening magnetic fields. For the propagation through the Galactic magnetic field, we use a lensing technique where particles of negative charge are backtracked from Earth to outside the Galaxy.
Extragalactic and Galactic magnetic fields deflect the UHECRs from their sources to Earth. The former fields are the least known, but assuming that they have a strength smaller than $\sim 10^{-9}$ G and a correlation length smaller than 1 Mpc [3, 31–33], the deflections of helium nuclei coming from the considered candidates at a distance less than 20 Mpc are negligible with respect to the deflections that occur during the propagation within our Galaxy.

The Galactic magnetic field can be further divided into regular and turbulent components. The regular part of the Galactic magnetic field is expected to give a dominant contribution to the UHECR deflections. There are several models of the regular Galactic field in the literature and there are large uncertainties (see e.g. [34–36]) so that their predictions cannot yet be used directly as an ingredient in the analysis. To test the sensitivities of the methods in this work, we chose to use the regular model of Jansson and Farrar [37], and two different scenarios for the turbulent component. One, from [38], has a “striated” random field (having the same orientation as the local coherent field but with a strength and sign which varies on a small scale) and a random Kolmogorov field with coherence length of 60 pc (referred to as “GMF-A” model). The model is empirical and data-driven, and the striated poloidal, toroidal and spiral components allow for effects such as a Galactic wind and the compression of an isotropic turbulent field. A second model for the random field is based on the analysis of the Planck team, which argues that the synchrotron emission map of WMAP used by [38] to fix the strength of the turbulent component of GMF-A is likely too large [39], and hence rescales the random field of [38] correspondingly. Therefore, we also simulate a weaker version of the turbulent field with the same coherence length but strength scaled-down by a factor 3, and without the striated field; we call this the “GMF-B” model.

To evaluate the sensitivity of the methods, we test scenarios where one of the source candidates, listed in Table 1, accelerates a certain number of cosmic rays, $N_s$, with an energy spectrum following a simple power law with $E^{-2}$. Two different scenarios are assumed for the chemical composition of the accelerated particles. In Scenario 1, the source accelerates helium nuclei with an energy between 40 EeV and 200 EeV. In Scenario 2, we assume that helium nuclei are accelerated with energies between 40 EeV to 80 EeV, and that there is a proton fraction between 20 EeV to 40 EeV. The number of accelerated helium nuclei is chosen to be, arbitrarily in this example, twice as high as the number of the proton events. These energy ranges were chosen assuming that the acceleration at the source follows a simple rigidity-dependent mechanism as expected from acceleration by electromagnetic fields. In Table 2, we show a brief summary of the chosen scenarios.

In both scenarios, we propagate the cosmic rays from the sources through GMF-A and GMF-B models. Hence, there are four simulation setups to be analyzed. We simulate a total number of events$^2$ $N_{tot} = 900$ above 40 EeV in Scenario 1, and $N_{tot} = 6000$ above 20 EeV in Scenario 2. In each simulation, each source candidate is studied separately, there are $N_s$ events originating in the chosen object, plus $N_{tot} - N_s$ isotropically distributed events, which follow the geometrical exposure of the Observatory and the measured energy spectrum. The arrival directions and energies of the $N_s$ events are simulated accounting for the experimental resolutions. Thus, we apply an experimental energy uncertainty$^3$ of 14% and an angular

---

$^2$These numbers are slightly smaller than the actual number of events in data, but the difference is expected to have a minor impact on the sensitivity results that are presented.

$^3$This is a worst-case scenario compared to the energy uncertainty reported in [16], which was found to be smaller than 9% for the energies considered, by making improvements in the calibration, atmospheric treatment, reconstruction, and invisible energy.
Figure 2. Examples of two simulations with $N_s = 50$ events from Cen A in Scenario 1, for the GMF-A (left) and the weaker version GMF-B (right), in Galactic coordinates.

resolution of $1^\circ$.

Table 2. Summary of the details of the scenarios chosen to study the sensitivity of the methods.

| Scenario 1 | Scenario 2 |
|------------|------------|
| Minimum Energy | 40 EeV | 20 EeV |
| Maximum Energy | 200 EeV | 80 EeV |
| Composition | He | p for $E < 40$ EeV; He for $E > 40$ EeV |
| GMF models | A and B | A and B |

In Figure 2, we show two examples of a simulation in Scenario 1, with Cen A as the source candidate, a number of injected signal cosmic rays of $N_s = 50$ and both Galactic magnetic field models GMF-A (left panel) and GMF-B (right panel), in Galactic coordinates.

5 Sensitivity studies

5.1 Sensitivity of the multiplets method

In this Section, we show the results of the sensitivity studies with the multiplet method, assuming the acceleration Scenario 1 (described in the previous Section 4), where helium nuclei are accelerated with energies between 40 EeV and 200 EeV. We perform 1000 simulations where a given $N_s$ source events are simulated from each source candidate.

For each simulation of $N_s$ events, the significance of the reconstructed multiplet is calculated by computing the fraction of simulations of isotropically distributed events (following the geometric exposure of the Observatory), with the same total number of events $N_{tot}$ and with the same energy spectrum, in which a multiplet with the same or larger multiplicity and passing the same cuts appears by chance.
When injecting $N_s$ events, the reconstructed multiplet does not necessarily have a multiplicity equal to $N_s$, since there can be simulated events that do not pass the required cuts, and there can be isotropically distributed events which align by chance with simulated ones from the chosen source. To account for this fact, in the sensitivity studies we present the mean chance probabilities computed as:

$$\langle P(N_s) \rangle = \sum_n f(n)P_{ch}(n),$$

where $f(n)$ is the fraction of $n$-plets obtained after having simulated $N_s$ source events and $P_{ch}(n)$ is the isotropic chance probability for a multiplet with $n$ or more events.

In the left panel of Figure 3, we present the mean chance probabilities for different cases of $N_s$ source events (shown with different markers), for the ten source candidates considered, in Scenario 1 and with the source events propagated through the GMF-A model. Due to the non-uniform exposure of the Observatory and to the dependence of the deflections and of the magnification in the Galactic magnetic field on the location of the source [40, 41], the number of events from the source required to obtained a mean chance probability corresponding to a 3σ level depends highly on the source candidate. For example, $N_s = 9$ injected cosmic rays for the sources M87 and NGC1068 are needed to reach a 3σ level, while $N_s = 18$ injected cosmic rays are needed for the source NGC4945. This corresponds to signal fractions of 1% and 2%, respectively.

In the right panel of Figure 3, we show a comparison of the two Galactic magnetic field models, GMF-A and GMF-B, for $N_s$ from 9 to 11. As expected, the multiplet method performs better for almost all source candidates with the GMF-B model, where the random deflections are weaker.

The values obtained for the number of events from the sources are reasonable. For instance, if we use the results published in [19] for the AGN and SBG models, the anisotropic fractions are $(7 \pm 4)\%$ and $(10 \pm 4)\%$, respectively. In the former case, if the three AGNs listed in Table 1 are the largest contributors, and if we assume that their relative flux contribution is the one shown in Figure 1, their respective contribution would be 6.8% for Cen A and ~0.1% for M87 and Fornax A. Translating these fractions to number of source events, it would mean...
Figure 4. Mean chance probability \( \langle P(N_s) \rangle \) for \( N_s = 10 \) as a function of the chosen source, for the GMF-A model and in Scenario 1. The different markers show the results for different values of the cuts \( C_{\text{min}} \) and \( W_{\text{max}} \). The dashed line indicates the one-sided 3\( \sigma \) chance probability.

\( N_s \approx 61 \) for Cen A and \( N_s \approx 0.8 \) and \( N_s \approx 0.9 \) for M 87 and Fornax A, respectively. If we compare to the sensitivity studies done for instance with GMF-A model (see the left panel of Figure 3), to obtain a mean \( p \)-value corresponding to a 3\( \sigma \) level, one would need \( N_s \approx 16 \) for Cen A, \( N_s \approx 9 \) for M 87 and \( N_s \approx 12 \) for Fornax A. Though the results are not as favorable for M 87 and Fornax A as they are for Cen A, their relative luminosity in UHECRs might not be proportional to their \( \gamma \)-ray luminosity as we assume here [42].

A similar comparison can be done with the SBG model. The number of events from the sources needed for a 3\( \sigma \) detection are well within the expectations from the results of [19] for the largest contributors, NGC 4945 and NGC 253 and not as much for NGC 1808 and NGC 4631, where less than one event is expected and \( N_s \) between 9 and 11 are needed (as it happens in the case of M 87 and Fornax A).

We should point out that the angular scales of 7\( ^\circ \) and 13\( ^\circ \), where the maximum deviation from isotropy was found in [19] for the AGN and SBG models, could be compatible with a He composition given the uncertainties on the GMF model. For example, using the simulations from Scenario 1, for all sources, at least 95\% of the events would be within the angular window for the SBG model. In the case of the AGN model, at least 40\% of the events would be contained within such an angular window for the ten sources, with six sources having a containment of at least 85\%.

Using the simulation of Scenario 1 with the GMF-A model and a number of injected source events of \( N_s = 10 \), we tested variations of the cuts on the correlation coefficient \( C_{\text{min}} \) and on the spread in the transverse direction of the multiplet \( W_{\text{max}} \). The mean chance probability \( \langle P(N_s) \rangle \) as a function of the chosen source, is shown in Figure 4. The original cuts of \( C_{\text{min}} = 0.9 \) and \( W_{\text{max}} = 1.5^\circ \) perform best for most sources. When making the cuts looser, more of the injected signal events can be recovered in the reconstructed multiplet. However, the significance of a larger multiplet passing looser bounds is not necessarily better than the significance of the smaller multiplet with stricter cuts, since in the former case, the probability of chance alignments in the isotropically distributed events also increases.

We studied the sensitivity of the method with Scenario 2. To perform the search in this scenario, we first searched for multiplets with events with energies above 40 EeV. After that, we selected the largest multiplet and we searched for events between 20 EeV and 40 EeV which would correlate with the events above 40 EeV. To pre-select these events, we chose...
those at an angular distance to the event with the highest energy in the multiplet expected if the deflection power was the one obtained with the higher energy events, with an uncertainty of 20%, assuming that the events between 20\;\text{EeV} and 40\;\text{EeV} were protons and those above 40\;\text{EeV} were He. We once more applied a cut to the maximum angular distance of 20° so that the linear approximation between \(1/E\) and the arrival directions is still expected to be valid. We simulated \(N_s = 10\) source events from each source candidate with energies above 40\;\text{EeV} and \(N_s = 5\) source events with energies between 20\;\text{EeV} and 40\;\text{EeV} and we compared the results to those obtained with Scenario 1 with the same number of source events \(N_s = 10\) above 40\;\text{EeV}. We present the results in Figure 5. Given the current statistics collected at the Pierre Auger Observatory, the sensitivity of the method is better in Scenario 1 when comparing it to Scenario 2, for the same number of source events above 40\;\text{EeV}. Hence, in this work, the method is only applied to events with energies above 40\;\text{EeV}.

### 5.2 Sensitivity of the thrust method

In the following the results of the sensitivity studies from the thrust ratio are presented for both introduced scenarios from Section 4, with energy thresholds of 20\;\text{EeV} and 40\;\text{EeV}. Again 1000 simulations are performed where \(N_s\) events are assigned to the respective source candidate. For each simulation, 100,000 arrival directions were drawn isotropically in every ROI for each of the 1000 simulations, where the identical number of cosmic rays follow the exposure in the ROI. By comparing the thrust ratio of the ROI with the distribution obtained with the isotropic realizations, we derive the isotropic chance probability \(p\).

First, we test the sensitivity of the observable with respect to the only free parameter, the radius of the region of interest \(r_{\text{ROI}}\). In Figure 6, we show the number of injected cosmic-ray source events \(N_s\) which leads to a 3\(\sigma\) significance to reject isotropy as a function of the parameter \(r_{\text{ROI}}\) for Scenario 1 in the left panel and Scenario 2 in the right panel. Different colors and markers indicate different source candidates from the catalog in Table 1. While there is an overall agreement of the sensitivity curves between Scenarios 1 and 2, the optimal choice for the parameter \(r_{\text{ROI}}\) depends strongly on the considered source candidate. This effect is due to the different deflection power of the Galactic magnetic field in the different

**Figure 5.** Mean chance probability \(\langle P(N_s)\rangle\) as a function of the chosen source. The black empty squares and asterisks are the results for Scenario 2, with \(N_s = 10\) above 40\;\text{EeV} and \(N_s = 5\) between 20\;\text{EeV} and 40\;\text{EeV}, for the two GMF models considered, respectively. The blue filled squares and empty circles are the results for Scenario 1, with \(N_s = 10\) above 40\;\text{EeV}, for the two GMF models considered, respectively. The dashed line indicates the one-sided 3\(\sigma\) chance probability.
regions of the sky resulting in patterns that are partially not covered within the ROI for a too small radius $r_{ROI}$. To obtain an overall good performance, we choose an intermediate radius of the ROI of $r_{ROI} = 0.3$ rad in the following.

In the next step, we study the sensitivity of the thrust ratio as a function of the number of injected signal cosmic rays $N_s$. In contrast to the multiplet method, the patterns produced by the source candidates have a larger impact on the sensitivity as can be seen by the large spread between the lines in Figure 7. In case of Scenario 1, with the 40EeV energy threshold, a relatively high number of $N_s \approx 30$ to $N_s \approx 60$ injected signal cosmic rays is needed to pass the $3\sigma$ confidence level, which corresponds to signal fractions between 3% and 6%. This performance is inferior to that of the multiplet search, where signal fractions of 1% to 2% are needed to reach the same confidence level. This difference is explained by the fact that the thrust ratio does not make a direct use of the energy information. The weaker turbulent magnetic field model GMF-B just yields a minor improvement on the performance: on average, the same sensitivity as in the case of GMF-A is reached when injecting two times less of signal cosmic rays.

For Scenario 2, with the 20EeV energy threshold and the GMF-A model, most of the targets reach the $3\sigma$ confidence level between $N_s \approx 40$ and $N_s \approx 60$ signal cosmic rays, corresponding to signal fractions between 0.7% and 1.0%, as can be seen in the right panel of Figure 7. The data above this energy threshold will only be analyzed with this method in the following.

**Figure 6.** Number of injected cosmic ray source events $N_s$, which leads to an one-sided $3\sigma$ chance probability as a function of the ROI radius $r_{ROI}$. Applied on the benchmark simulation with the stronger GMF-A model, for Scenario 1 ($E > 40$EeV) on the left panel and Scenario 2 ($E > 20$EeV) on the right panel.
Figure 7. Expected sensitivity for the thrust ratio observable on the benchmark simulation with the stronger GMF-A model, for Scenario 1 \((E > 40\text{ EeV})\) on the left panel and Scenario 2 \((E > 20\text{ EeV})\) on the right panel. The red line indicates the 3σ confidence level.

6 Results of the targeted search

In this Section, we present the results of the targeted search with the source candidates listed in Table 1, applying the multiplet and thrust methods to the data collected at the Pierre Auger Observatory described in Section 2.

The results are shown in Table 3 for each candidate, for the multiplet search with an energy threshold of 40EeV, and for the thrust ratio with energy thresholds of 20EeV and 40EeV. All the probabilities found with respect to an isotropic distribution of arrival directions are above 1%, thus no significant signature of an alignment pattern around the chosen targets could be found. These probabilities are not penalized for the trial of ten different candidates.

Table 3. Isotropic chance probabilities for the targeted search with the multiplet and thrust ratio methods applied to data collected at the Pierre Auger Observatory. These probabilities are not penalized for the use of ten different candidates.

| Target       | Multiplets (40EeV) | Thrust ratio (20EeV) | Thrust ratio (40EeV) |
|--------------|--------------------|----------------------|----------------------|
| Cen A        | \(1.2 \times 10^{-2}\) | 0.75                 | 0.42                 |
| M87          | 0.61               | 0.44                 | 0.85                 |
| Fornax A     | 0.96               | 0.21                 | \(1.9 \times 10^{-2}\) |
| NGC 253      | 0.54               | 0.98                 | 0.88                 |
| NGC 4945     | 0.25               | \(2.9 \times 10^{-2}\) | \(3.7 \times 10^{-2}\) |
| Circinus     | 0.99               | 0.82                 | 0.58                 |
| M83          | 0.20               | 0.14                 | 0.54                 |
| NGC 4631     | —                  | 0.59                 | 0.85                 |
| NGC 1808     | 0.61               | 0.63                 | 0.77                 |
| NGC 1068     | 0.75               | \(6.0 \times 10^{-2}\) | 0.29                 |

The most interesting but non-significant result for the multiplet search, with \(E > 40\text{ EeV}\), is with Cen A as source candidate, where an 8-plet is found with a chance probability of 1.2% with respect to isotropic expectations. The fitted deflection power is \(D = (9 \pm 2)° \times 100\text{ EeV}\).
In the upper left panel of Figure 8, we visualize the arrival directions of the events that form the 8-plet.

In the case of the thrust ratio observable, the smallest $p$-values are found with the source candidates Fornax A (with $E > 40$ EeV), NGC 4945 (with both energy thresholds) and NGC 1068 (with $E > 20$ EeV), with chance probabilities between 1.9% and 6.0%. There is barely any overlap between the cosmic rays within the multiplet of the Cen A region and the region of interest evaluated for the thrust observable. In the upper right panel of Figure 8, we present the arrival directions of the events in the ROI centered on Fornax A above 40 EeV. The strong response of the thrust ratio ($T_2/T_3 = 1.686$) seems to be an artifact of an asymmetric event distribution in the ROI rather than a promising deflection signature. The lower panel of Figure 8 shows the candidates NGC 4945 and NGC 1068 for energies above 20 EeV.

It is instructive to look at the lack of magnetically-induced structure in the light of the other measurements carried out at the Observatory. Assuming that the GMF models used in our simulations are a good approximation of the actual one, and considering the anisotropic fractions obtained in [19] for the AGN and SBG models, we should have detected a significant signal in the multiplets and thrust searches if all the events coming from the sources are light elements (p or He). For instance, in the case of Cen A, for a total number of 1119 events, ~76 events would have been expected from this source. However, the putative multiplet found with Cen A as source candidate has a multiplicity of 8 events only. Thus, under these assumptions, the lack of a significant high-multiplicity signal appears to be consistent with a scenario where less than ~10% of cosmic rays above 40 EeV are light elements. Such a fraction is in line with our composition constraints at the highest energies [4, 5]. Overall, the various facets of our data are thus consistent.

7 Results of the all-sky blind search

We also evaluate both methods on the entire sky, for the multiplet method above energies of 40 EeV and for the thrust method for both energy thresholds, 40 EeV and 20 EeV.

The largest multiplet found has a multiplicity of 10 which may appear by chance from an isotropic distribution of events with a probability of 11.4%. The second largest multiplet has a multiplicity of 9 events. The chance probability of finding at least 2 multiplets with multiplicity larger than or equal to 9 in isotropic simulations is 19.1%. The respective deflection power values are $D = (8.0 \pm 1.3)° \times 100$ EeV and $D = (12 \pm 2)° \times 100$ EeV. The arrival directions of the events that form the 10-plet and 9-plet are shown in the left panel of Figure 9, as well as the position of what would be their reconstructed source.

When searching for 8-plets, seven independent ones were found. We define “independent” multiplets those sets of events that have less than half the number of events in the set in common with others. The chance probability of finding at least 9 multiplets with multiplicity larger than or equal to 8 in simulations of isotropic arrival directions is 5.6%. Thus, no statistically significant results were found. In the right panel of Figure 9, we present the arrival directions of the events in all the 8-plets as well as the reconstructed positions of their potential sources.

For the thrust ratio observable, we used the HEALPix scheme [44] to locate the ROIs equally on the sphere. For each ROI, isotropic realizations with the same number of cosmic rays following the geometrical exposure within the ROI were used to determine local $p$-values. Then, the lowest local $p$-value in the sky is compared with the lowest local $p$-values of 10,000 isotropic skies to determine the post-trial significance. To overcome computational issues,
Figure 8. Arrival directions of events in Galactic coordinates from chosen sky regions which yield the smallest isotropic chance probabilities in Table 3. The upper row shows the AGN candidates CenA with the 8-plet from the multiplet method (left) and FornaxA with the thrust ratio (right), both for the energy threshold of 40 EeV. The lower row shows the SBG candidates NGC4945 (left) and NGC1068 (right) evaluated with the thrust ratio on the energy threshold of 20 EeV. The red bars show the thrust vectors $T_2 \cdot \hat{n}_2$ (solid) and $T_3 \cdot \hat{n}_3$ (dashed) as defined in Section 3.2.

The isotropic distributions for the thrust ratio observable have been parametrized and pre-calculated on a grid of equatorial declinations and number of cosmic rays within the ROI (cf. Appendix). We select only ROIs with declination lower than $+20^\circ$ and a cosmic ray number of at least 15 to guarantee a sufficiently accurate parametrization.

The lowest but non-significant isotropic chance probability for the thrust ratio observable was found for the energy threshold of 20 EeV with a ROI centered at Galactic longitude $\ell = -9.8^\circ$ and Galactic latitude of $b = -17.0^\circ$. The corresponding thrust-ratio was found to be $T_2 / T_3 = 1.362$ which translates to a post-trial $p$-value of 25%. For the higher energy threshold of 40 EeV, we obtained a post-trial $p$-value of 46.7% with a thrust-ratio of $T_2 / T_3 = 2.703$. With the ROI centered at $\ell = -151.9^\circ$ and $b = -54.3^\circ$, we found the same artifact of an
Figure 9. Arrival directions in Galactic coordinates of the events that form the 10-plet and 9-plet (left) and 8-plets (right) found on the all-sky blind search with the multiplets method with an energy threshold of $E > 40\,\text{EeV}$. The radius of the circles is proportional to the energy of the event. Plus signs indicate the positions of the potential sources for each multiplet. The dashed line represents the Equatorial plane.

Blind search
\[
\frac{T_2}{T_3} = 2.703
\]

\[
\begin{align*}
&-160^\circ \pm 140^\circ \\
&-50^\circ \pm 30^\circ
\end{align*}
\]

\[
\begin{align*}
&10^{19.7} \quad 10^{19.9} \quad 10^{20.1}
\end{align*}
\]

Figure 10. Arrival directions of events in Galactic coordinates inside the ROI located in the direction which yields the smallest local $p$-value in the all-sky blind search for the energy thresholds of $40\,\text{EeV}$ (left) and $20\,\text{EeV}$ (right).

Blind search
\[
\frac{T_2}{T_3} = 1.362
\]

\[
\begin{align*}
&-20^\circ \pm 0^\circ \\
&-30^\circ \pm 10^\circ
\end{align*}
\]

\[
\begin{align*}
&10^{19.4} \quad 10^{19.7} \quad 10^{20.0}
\end{align*}
\]

unevenly filled ROI close to the Fornax A region (cf. Section 6).

8 Conclusions

Using a set of UHECRs collected at the Pierre Auger Observatory, with an exposure of 101,900 km$^2$ sr yr, we searched for indications of magnetically-induced signatures in the arrival directions of the events. We applied two different methods: a search for multiplets and the thrust method. We performed both a search using a list of astrophysical sources, candidates to
be sites of UHE acceleration, and an all-sky blind search. We found no statistically significant feature with any of the methods for the energy thresholds considered, 40 EeV for the multiplets method and 20 EeV and 40 EeV for the thrust one. The largest deviations from isotropic expectations were found with a $p$-value of 1.9% around the Fornax A region for the thrust search above 40 EeV and with a $p$-value of 1.2% around the Cen A region for the multiplet search above 40 EeV. Given the state of the art of the Galactic magnetic field models, the lack of signal is along the lines of a scenario where less than $\sim$10% of cosmic rays above 40 EeV are light elements, which is consistent with our composition constraints at the highest energies.

Future measurements will allow for disentangling of the electromagnetic and muonic components on an event-by-event basis with the upgraded version of the Pierre Auger Observatory [43]. Ultimately, the analyses presented in this study will benefit from these measurements which will enable an accurate analysis of mass-sensitive parameters for each event.

Acknowledgments

The successful installation, commissioning, and operation of the Pierre Auger Observatory would not have been possible without the strong commitment and effort from the technical and administrative staff in Malargüe. We are very grateful to the following agencies and organizations for financial support:

Argentina – Comisión Nacional de Energía Atómica; Agencia Nacional de Promoción Científica y Tecnológica (ANPCyT); Consejo Nacional de Investigaciones Científicas y Técnicas (CONICET); Gobierno de la Provincia de Mendoza; Municipalidad de Malargüe; NDM Holdings and Valle Las Leñas; in gratitude for their continuing cooperation over land access;

Australia – the Australian Research Council; Brazil – Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq); Financiadora de Estudos e Projetos (FINEP); Fundação de Amparo à Pesquisa do Estado de Rio de Janeiro (FAPERJ); São Paulo Research Foundation (FAPESP) Grants No. 2019/10151-2, No. 2010/07359-6 and No. 1999/05404-3; Ministério da Ciência, Tecnologia, Inovações e Comunicações (MCTIC); Czech Republic – Grant No. MSMT CR LTT18004, LM2015038, LM2018102, CZ.02.1.01/0.0/0.0/16_013/0001402, CZ.02.1.01/0.0/0.0/18_046/0016010 and CZ.02.1.01/0.0/0.0/17_049/0008422; France – Centre de Calcul IN2P3/CNRS; Centre National de la Recherche Scientifique (CNRS); Conseil Régional Ile-de-France; Département Physique Nucléaire et Corpusculaire (PNC-IN2P3/CNRS); Département Sciences de l’Univers (SDU-INSU/CNRS); Institut Lagrange de Paris (ILP) Grant No. LABEX ANR-10-LABX-63 within the Investissements d’Avenir Programme Grant No. ANR-11-IDEX-0004-02; Germany – Bundesministerium für Bildung und Forschung (BMBF); Deutsche Forschungsgemeinschaft (DFG); Finanzministerium Baden-Württemberg; Helmholtz Alliance for Astroparticle Physics (HAP); Helmholtz-Gemeinschaft Deutscher Forschungszentren (HGF); Ministerium für Innovation, Wissenschaft und Forschung des Landes Nordrhein-Westfalen; Ministerium für Wissenschaft, Forschung und Kunst des Landes Baden-Württemberg; Italy – Istituto Nazionale di Fisica Nucleare (INFN); Istituto Nazionale di Astrofisica (INAF); Ministero dell’Istruzione, dell’Università e della Ricerca (MIUR); CETEMPS Center of Excellence; Ministero degli Affari Esteri (MAE); México – Consejo Nacional de Ciencia y Tecnología (CONACYT) No. 167733; Universidad Nacional Autónoma de México (UNAM); PAPIIT DGAPA-UNAM; The Netherlands – Ministry of Education, Culture and Science; Netherlands Organisation for Scientific Research (NWO); Dutch national e-infrastructure with the support of SURF Cooperative; Poland – Ministry of Science and Higher Education, grant No. DIR/WK/2018/11; National Science
Centre, Grants No. 2013/08/M/ST9/00322, No. 2016/23/B/ST9/01635 and No. HARMO-
NIA 5-2013/10/M/ST9/00062, UMO-2016/22/M/ST9/00198; Portugal – Portuguese na-
tional funds and FEDER funds within Programa Operacional Factores de Competitividade
through Fundação para a Ciência e a Tecnologia (COMPETE); Romania – Romanian Ministry of
Education and Research, the Program Nucleu within MCI (PN19150201/16N/2019 and
PN19060102) and project PN-III-P1-1.2-PCCDI-2017-0839/19PCCDI/2018 within PNCDI
III; Slovenia – Slovenian Research Agency, grants P1-0031, P1-0385, I0-0033, N1-0111; Spain –
Ministerio de Economía, Industria y Competitividad (FPA2017-85114-P and FPA2017-85197-
P), Xunta de Galicia (ED431C 2017/07), Junta de Andalucía (SOMM17/6104/UGR), Feder
Funds, RENATA Red Nacional Temática de Astropartículas (FPA2015-68783-REDT) and
María de Maeztu Unit of Excellence (MDM-2016-0692); USA – Department of Energy, Con-
tracts No. DE-AC02-07CH11359, No. DE-FR02-04ER41300, No. DE-FG02-99ER41107 and
No. DE-SC0011689; National Science Foundation, Grant No. 0450696; The Grainger Foun-
dation; Marie Curie-IRSES/EPLANET; European Particle Physics Latin American Network;
and UNESCO.

Appendix

The distribution of the thrust-ratio observable for an isotropic arrival distribution and an
energy spectrum as measured by the Pierre Auger Observatory can be described by the
density function

$$f(t; a, b) = \frac{a^{3/b} b}{\Gamma(3/b)} (t - 1)^2 \exp(-a(t - 1)^b),$$

(8.1)

where $t = T_2/T_3$ is the thrust ratio, $\Gamma(x)$ is the Gamma function and $a$ and $b$ are fit parameters.

For both scenarios presented in Section 4, the density function (8.1) has been fitted to $T_2/T_3$-
distributions as resulting from isotropically distributed cosmic rays. The parameters $a$ and
$b$ of this density function depend only on two variables, the equatorial declination $\delta_{ROI}$
of the ROI center and the number of cosmic rays within the ROI, $N_{ROI}$. We evaluated
$a$ and $b$ of the density function for 30 different declinations $\delta_{ROI}$ ranging from $-90^\circ$ to $+45^\circ$
and for each of them for 25 different cosmic-ray numbers $N_{ROI}$ ranging from $-4$ to $+4$ standard
deviations in the Poissonian distribution, which depend on the integrated exposure within
the ROI. For sufficiently high cosmic-ray numbers $N_{ROI}$ (above 15 events), we find that the
parameter $a$ is highly correlated to the parameter $b$ as $a = 3.59 \exp(0.831 b^4) + 2.73$. For any
continuous value of the equatorial declination $\delta_{ROI}$ and the number of cosmic rays $N_{ROI}$, we
use a 2-dimensional interpolation algorithm to determine the parameter $a$ and calculate the
local $p$-value with the analytical integral of Equation (8.1),

$$p_{val} = \int_{t}^{\infty} f(x; a, b) dx = \frac{\Gamma_i(3/b, a(t - 1)^b)}{\Gamma(3/b)},$$

(8.2)

where $\Gamma_i(x, y)$ is the incomplete upper Gamma function.

References

[1] J.L. Han, Observing Interstellar and Intergalactic Magnetic Fields, Annu. Rev. Astron.
Astrophys. 55 (2017) 111-57.
[2] R. Beck, R. Wielebinski, *Magnetic Fields in Galaxies*, Chapter 13 in "Planets, Stars and Stellar Systems", Vol. 5: “Galactic Structure and Stellar Populations”, ed. G. Gilmore, Springer, Berlin 2013, ISBN 978-90-481-8817-8 [arXiv:1302.5663].

[3] R. Durrer, A. Neronov, *Cosmological Magnetic Fields: Their Generation, Evolution and Observation*, Astron. Astrophys. Rev. 21 (2013) 62 [arXiv:1303.7121].

[4] A. Aab et al. [The Pierre Auger Collaboration], *Depth of Maximum of Air-Shower Profiles at the Auger Observatory: Measurements at Energies above 10^{17.8} eV*, Phys. Rev. D 90 (2014) 122005 [arXiv:1409.4809].

[5] A. Aab et al. [The Pierre Auger Collaboration]. *Depths of Maximum of Air-Shower Profiles at the Pierre Auger Observatory: Composition Implications*, Phys. Rev. D 90 (2014) 122006 [arXiv:1409.5083].

[6] A. Yushkov for the Pierre Auger Collaboration, *Mass composition of cosmic rays with energies above 10^{17.2} eV from the hybrid data of the Pierre Auger Observatory*, PoS (ICRC2019) 482 [arXiv:1909.09073].

[7] J.P. Lundquist and P.V. Sokolsky for the Telescope Array Collaboration, *Supergalactic Structure of Multiplets with the Telescope Array Surface Detector*, EPJ Web Conf. 210 (2019) 01006

[8] P. Abreu et al. [The Pierre Auger Collaboration], *Search for signatures of magnetically-induced alignment in the arrival directions measured by the Pierre Auger Observatory*, Astropart. Phys. 35 (2012) 354-361 [arXiv:1111.2472].

[9] A. Aab et al. [The Pierre Auger Collaboration], *Search for patterns by combining cosmic ray energy and arrival directions at the Pierre Auger Observatory*, Eur. Phys. J. C 75 (2015), 269 [arXiv:1410.0515].

[10] J. Abraham et al. [The Pierre Auger Collaboration], *Properties and performance of the prototype instrument for the Pierre Auger Observatory*, Nucl. Instrum. Meth. A 523 (2004) 50.

[11] A. Aab et al. [The Pierre Auger Collaboration], *The Pierre Auger Cosmic Ray Observatory*, Nucl. Instrum. Meth. A 798 (2015) 172 [arXiv:1502.01323].

[12] C. Bonifazi for the Pierre Auger Collaboration, *The angular resolution of the Pierre Auger Observatory*, Nucl. Phys. B Proc. Suppl. 190 (2009) 20 [arXiv:0901.3138].

[13] D. Mockler for the Pierre Auger Collaboration, *Reconstruction of Vertical Events Recorded by the Surface Detector of the Pierre Auger Observatory*, PoS (ICRC2019) 353 [arXiv:1909.09073].

[14] M. Ave for the Pierre Auger Collaboration, *Reconstruction accuracy of the surface detector array of the Pierre Auger Observatory*, Proc. of the 30th Int. Cosmic Ray Conf. (2007) 4 307, [arXiv:0709.2125].

[15] A. Aab et al. [The Pierre Auger Collaboration], *Reconstruction of inclined air showers detected with the Pierre Auger Observatory*, J. Cosmology & Astropart. Phys. 8 (2014) 19 [arXiv:1407.3214].

[16] B.R. Dawson for the Pierre Auger Collaboration, *The Energy Scale of the Pierre Auger Observatory*, PoS (ICRC2019) 231 [arXiv:1909.09073].

[17] J. Abraham et al. [The Pierre Auger Collaboration], *Trigger and aperture of the surface detector array of the Pierre Auger Observatory*, Nucl. Instrum. Meth. A 613 (2010) 29 [arXiv:1111.6764].

[18] G. Golup, D. Harari, S. Mollerach, E. Roulet, *Source position reconstruction and constraints on the galactic magnetic field from ultra-high energy cosmic rays*, Astropart. Phys. 32 (2009) 269-277 [arXiv:0902.1742].
[19] A. Aab et al. [The Pierre Auger Collaboration], *An indication of anisotropy in arrival directions of ultra-high-energy cosmic rays through comparison to the flux pattern of extragalactic gamma-ray sources*, Astrophys. J. Lett. 853 (2018), 2 [arXiv:1801.06100].

[20] M. Ackermann et al., *2FHL: the second catalog of hard Fermi-LAT sources*, Astrophys. J. Suppl. Ser. 222 (2016) 5 [arXiv:1508.04449].

[21] M. Ackermann et al., *GeV observations of star-forming galaxies with the Fermi Large Area Telescope*, Astrophys. J. 755 (2012) 164 [arXiv:1206.1346].

[22] M. Ajello et al., *3FHL: The Third Catalog of Hard Fermi-LAT Sources*, Astrophys. J. 232 (2017) 2 [arXiv:1702.00664].

[23] J.K. Becker, P.L. Biermann, J. Dreyer, T.M. Kneiske, *Cosmic Rays VI-Starburst galaxies at multiwavelengths*, [arXiv:0901.1775].

[24] L. Caccianiga for the Pierre Auger Collaboration, *Anisotropies of the highest energy cosmic-ray events recorded by the Pierre Auger Observatory in 15 years of operation*, PoS (ICRC2019) 206 [arXiv:1909.09073].

[25] R.U. Abbasi et al. [The Telescope Array Collaboration], *Testing a Reported Correlation between Arrival Directions of Ultra-high-energy Cosmic Rays and a Flux Pattern from nearby Starburst Galaxies using Telescope Array Data*, Astrophys. J. Lett. 867 (2018), 2.

[26] R.B. Tully et al., *COSMICFLOWS-2: the data*, Astronom. J. 146 (2013) 4 [arXiv:1307.7213].

[27] R.B. Tully et al., *Our Peculiar Motion Away from the Local Void*, Astrophys. J. 676 1 (2008) 184-205 [arXiv:0705.4139].

[28] M. Cappellari et al., *The ATLAS3D project - I. A volume-limited sample of 260 nearby early-type galaxies: science goals and selection criteria*, Mon. Not. R. Astron. Soc. 413 2 (2011) 813-836 [arXiv:1012.1551].

[29] R.B. Tully, L. Rizzi, E.J. Shaya and H.M. Courtois, D.I. Makarov, B.A. Jacobs, *The Extragalactic Distance Database*, arXiv:0902.3668.

[30] H. P. Bretz, M. Erdmann, P. Schiffer, D. Walz, T. Winchen, *PARSEC: A Parametrized Simulation Engine for Ultra-High Energy Cosmic Ray Protons*, Astropart. Phys. C54 (2014) 110 [arXiv:1302.3761].

[31] P.P. Kronberg, *Extragalactic magnetic fields*, Rept. Prog. Phys. 57 (1994) 325.

[32] M.S. Pshirkov, P.G. Tinyakov and F.R. Urban, *New Limits on Extragalactic Magnetic Fields from Rotation Measures*, Phys. Rev. Lett. 116, 191302 (2016) [arXiv:1504.06546].

[33] K. Subramanian, *From Primordial Seed Magnetic Fields to the Galactic Dynamo*, Galaxies 7 (2019) 47 [arXiv:1903.03744].

[34] G.R. Farrar, *The Galactic Magnetic Field and Ultrahigh-Energy Cosmic Ray Deflections*, C. R. Physique XX (2014) [arXiv:1405.3680].

[35] M. Erdmann, G. Müller, M. Urban, M. Wirtz, *The Nuclear Window to the Extragalactic Universe*, Astropart. Phys. 85 (2016) 54-64 [arXiv:1607.01645].

[36] M. Unger, G.R. Farrar, *Progress in the Global Modeling of the Galactic Magnetic Field*, EPJ Web of Conferences 210 (2019) 04005 [arXiv:1901.04720].

[37] R. Jansson, G.R. Farrar, *A New Model of the Galactic Magnetic Field*, Astrophys. J. 757 (2012), 14 [arXiv:1204.3662].

[38] R. Jansson, G.R. Farrar, *The Galactic Magnetic Field*, Astrophys. J. 761 (2012), L11 [arXiv:1210.7820].

[39] R. Adam [Planck Collaboration], *Planck intermediate results. XLII. Large-scale Galactic magnetic fields*, Astron. Astrophys. 596 (2016) A103 [arXiv:1601.00546].
[40] D. Harari, S. Mollerach, E. Roulet, The toes of the ultrahigh-energy cosmic ray spectrum, J. High Energy Phys. 9908 (1999) 022 [arXiv:astro-ph/9906309].

[41] G.R. Farrar, M.S. Sutherland, Deflections of UHECRs in the Galactic magnetic field, J. Cosmol. Astropart. Phys. 1905 (2019) 05 004 [arXiv:1711.02730].

[42] J.H. Matthews, A.R. Bell, K.M. Blundell, A.T. Araudo, Fornax A, Centaurus A, and other radio galaxies as sources of ultrahigh energy cosmic rays, Mon. Not. R. Astron. Soc. 479 (2018) 1 L76-L80 [arXiv:1805.01902].

[43] A. Castellina for the Pierre Auger Observatory, AugerPrime: the Pierre Auger Observatory Upgrade, EPJ Web Conf. 210 (2019) 06002.

[44] K. Gorski, E. Hivon, A. Banday, et al., HEALPix: A Framework for High-Resolution Discretization and Fast Analysis of Data Distributed on the Sphere, Astrophys. J. 622 759 (2005) 771.