Triple-mode squeezing with dressed six-wave mixing

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The theory of proof-of-principle triple-mode squeezing is proposed via spontaneous parametric six-wave mixing process in an atomic-cavity coupled system. Special attention is focused on the role of dressed state and nonlinear gain on triple-mode squeezing process. Using the dressed state theory, we find that optical squeezing and Autler-Towns splitting of cavity mode can be realized with nonlinear gain, while the efficiency and the location of maximum squeezing point can be effectively shaped by dressed state in atomic ensemble. Our proposal can find applications in multi-channel communication and multi-channel quantum imaging.

Generating squeezed vacuum and entanglement with controllable quantum states is important to quantum communication, quantum information processing and quantum computation1–3. For example, the single-mode quadrature squeezed state is used for gravity wave detection, which is produced by the highly refined optical parametric oscillators (OPOs)4. The linear optical processing of single-beam quadrature squeezed states is used for the continuous-variable quantum computing5,6. The multi-spatial mode squeezed light is desirable to continuous-variable quantum image processing techniques7,8. Generally speaking, techniques for producing the squeezing states are based on either parametric down conversion in solid state crystal or spontaneous parametric four-wave mixing (SP-FWM) schemes in atomic vapors. Traditionally, biphotons generated from Spontaneous parametric down-conversion (SPDC) in nonlinear crystals have very wide bandwidth (THz) and ultra-short coherence time (ps)9,10.

Using four-wave mixing (FWM) in sodium vapor, squeezed state of light was experimentally implemented11–13, however, achieving higher degree of squeezing via FWM in atomic vapors is limited by spontaneous emission noise. Recently, researches on FWM in atomic vapors demonstrated that the spontaneous emission noise can be reduced or eliminated by using of electromagnetically induced transparency (EIT)14. In EIT window the transmission1, slowing down15–17, and storage and retrieval18–19 of squeezed states were also experimentally demonstrated. Nowadays, the interest to generate triple-mode squeezing is mainly due to its applicability in quantum information and communication20–21 where the field fluctuations in one of the quadratures are reduced below the vacuum noise level, and can be used in overcoming the shot-noise precision restrictions in optical measurements22 and enhancing the capacity of communication channels23. Usually, signal-to-noise ratio is very low for six-wave mixing (SWM) in atomic vapor. However, by employing two-photon Doppler-free configurations as well as EIT, enhanced nonlinear processes due to atomic coherence have been experimentally demonstrated24. The essentials of such enhanced nonlinear optical processes are the enhanced nonlinear susceptibility due to atomic coherence, slowed light beam propagation in the atomic medium, and greatly reduced linear absorption of the generated optical field due to EIT, which enable us to investigate the topological photonic problems in atomic ensembles25,26.

In our previous studies, distinctly different from and advantageous over the previously reported27, highly efficient FWM, SWM, and eight-wave mixing processes was experimentally demonstrated in an open-cycle Y-type atomic system. By manipulating the atomic coherence and multi-photon interferences among different energy levels, we also demonstrated that the third-order and fifth-order nonlinear processes can coexist in open (such as V-type, Y-type, and inverted Y-type) atomic systems24, and the SWM signal can be comparable with or even greater than the FWM signal in amplitude. Such coexisting processes allow us to investigate spatial-temporal coherent interference between third-order and fifth-order nonlinear processes. We also demonstrated the parametrically amplified FWM (PA-FWM) and parametrically amplified SWM (PA-SWM) processes. Such enhanced
nonlinear process is used to generate the strongly correlated bright twin or triple-mode bright beams in cavity and free space with high efficiency and narrow band width.

In this paper, by applying dressed state theory, we examine the influence of dressed state and nonlinear gain on the triple-mode squeezing via three-mode cone emission of SP-SWM, and single-mode and two-mode squeezing via degenerate and nondegenerate self-diffraction (or phase-conjugate) cone emissions of SP-FWM. It is indicated that the optical squeezing and nonlinear Autler-Towns (AT) splitting of quantum noise can be achieved via nonlinear gain. The profiles and location of maximum squeezing point can be effectively modulated by dressed state, that can be achieved only in atomic media. The triple-mode squeezing state proposed in current work can be directly used in multichannel quantum imaging. The quality of imaging (e.g. the contrast and resolution) is significantly improved, compared with that obtained by using the two-mode squeezing state. In addition, the work can be used as implementation of triple-mode entangled source, where the generation efficiency of entangled triple-beam and degree of entanglement will be significantly enhanced by nonlinear susceptibility and quantum gain. Therefore, our scheme can be also used to achieve multi-channel communication. Finally, by using SP-SWM both in cold and hot atomic ensembles, narrow-band triple-photons with a long coherence time is realized. Such a long coherence time may allow us to access and manipulate the squeezed state directly, and has potential application in the long-distance quantum communication.

So our scheme has following advantages. First, due to the near- and on-resonance nonlinear optical processes can be enhanced by atomic coherence technique, so the generation efficiency of SP-SWM and degree of triple of squeezing (entanglement) can be significantly enhanced by manipulating nonlinear susceptibility and quantum gain. Second, due to EIT window (MHz), not only the resonance absorption is eliminated, but narrow bandwidth signals at low light level is obtained as well. So compared with correlated photon pairs from SPDC, which have characteristics of very wide bandwidth (THz) and ultra-short coherence time (ps). Our scheme has a narrower-bandwidth (MHz) and longer coherence time (0.1–1.0 μs). Last but not least, the quality of imaging can be well controlled by multiple parameters.

**Basic Theory of Triple-Mode Cone Emission**

A theoretical scheme for the preparation triple-mode by SP-SWM is carried out in 85Rb atomic ensemble. As shown in Fig. 1(a), the energy levels of 5S1/2(F = 3), 5P3/2(F = 3), 5D5/2, and 5S1/2(F = 2) forming the reverse Y-type four-level atomic system are corresponding to |0⟩, |1⟩, |2⟩, and |3⟩, respectively. In this energy level system, three high intensity pumping fields \( E_0 \), \( E_1 \), and \( E_2 \) are used to coupling with \( |0⟩ \rightarrow |1⟩, |1⟩ \rightarrow |2⟩ \) and \( |3⟩ \rightarrow |1⟩ \), respectively. Therefore, non-degenerate SP-SWM process is excited and three quantum correlated signals \( Eictions/3, E_2, \text{and } E_3 \) are generated, satisfies the phase-matching condition \( k_1 + k_2 + k_3 = k_{31} + k_{32} + k_{33} \), as the phase-matching ring configuration shown in Fig. 1(a).
In this reverse Y-type system, via the perturbation chain $\rho_{00}^{(0)} \rightarrow \rho_{10}^{(1)} \rightarrow \rho_{10}^{(2)} \rightarrow \rho_{10}^{(3)} \rightarrow \rho_{10}^{(4)} \rightarrow \rho_{10}^{(5)}$, the density matrix element $\rho_{10}^{(5)}$ for the generated signal $E_{31}$ can be obtained as

$$\rho_{10}^{(5)} = \frac{iG_3G_2G_1G_0^*}{d_{10}d_{01}d_{02}d_{03}d_{10}d_{12}d_{13}},$$

where $G_i = \mu E_i/h$ is the Rabi frequency, here $\mu_i$ is electric dipole moment between energy state $|i\rangle$ and $|j\rangle$, and $\Gamma_j$ is the transverse decay rate, $d_{10} = \Gamma_{10} + i\Delta_{10}$, $d_{03} = \Gamma_{03} + i\Delta_{03}$, $d_{12} = \Gamma_{12} + i\Delta_{12}$. Similarly, we can obtain $\rho_{20}^{(5)}$ and $\rho_{30}^{(5)}$ for $E_{30}$ and $E_{30}$ via the perturbation chains $\rho_{00}^{(0)} \rightarrow \rho_{01}^{(1)} \rightarrow \rho_{01}^{(2)} \rightarrow \rho_{01}^{(3)} \rightarrow \rho_{01}^{(4)} \rightarrow \rho_{01}^{(5)}$ and $\rho_{00}^{(0)} \rightarrow \rho_{02}^{(1)} \rightarrow \rho_{02}^{(2)} \rightarrow \rho_{02}^{(3)} \rightarrow \rho_{02}^{(4)} \rightarrow \rho_{02}^{(5)}$, and the corresponding expressions for $E_{32}$ and $E_{33}$ are

$$\rho_{20}^{(5)} = \frac{iG_3G_2G_1G_0^*}{d_{20}d_{10}d_{12}d_{13}},$$

$$\rho_{30}^{(5)} = \frac{iG_3G_2G_1G_0^*}{d_{30}d_{10}d_{12}d_{13}}.$$

The fluctuations of the triple-modes $E_{31}, E_{32}, E_{33}$ generated here have zero on average and quantum correlated with each other. That is to say, if there is no seeding to this SP-SWM process, the output states are the triple-mode squeezed vacuum states. By adjusting one of the SP-SWMs, the other two will be affected. For the SP-SWM, as shown in Fig. 2(a), any one of the three polar angles ($\phi_{31}$, $\phi_{32}$ or $\phi_{33}$) can be represented by the other two, and we cannot get the dependent phase mismatching conditions for $E_{31}$, $E_{32}$ or $E_{33}$, which is much more complex than the self-diffraction and phase-conjugate SP-FWM cases. In order to investigate the quantum-correlated of three-photon cone emissions, we fix the polar angle of $k_{30}$ to be $\phi_{30}^0$, which does not affect the other two polar angles ($\phi_{31}$, and $\phi_{32}$) to be fixed relatively. According to the configuration shown in Fig. 2(a), we can get the phase mismatching conditions for $E_{31}$ and $E_{32}$ as following,

$$\Delta k_{31} = k_1 - k_2 + k_3 - k_{31} \cos(\phi_{31}) - k_{32} \cos(\phi_{32}) - \sqrt{k_{31}^2 - [k_{31} \sin(\phi_{31}) + k_{32} \sin(\phi_{32})]^2},$$

$$\Delta k_{33} = k_1 - k_2 + k_3 - \sqrt{k_{31}^2 - [k_{31} \sin(\phi_{31}) + k_{32} \sin(\phi_{32})]^2} - k_{32} \cos(\phi_{32}) - k_{33} \cos(\phi_{33}).$$

As we know that the fifth-order nonlinear susceptibility highest if the incident light is set collinear $\phi_{32} = \phi_{33} = 0$, so the nonlinear conversion efficiency is the highest as collinear. However, the generated SP-SWM is buried in strong fluorescence background due to the resonance fluorescence signal is also strongest in this.
direction. To ensure high conversion efficiency of SP-SWM and suppressed collinear resonance fluorescence, so we set $\phi_{S2} = \phi_{S3} = 2.9$. By setting $\varphi_{S1} = \varphi_{S2} = 2.9$, now we can investigate SP-SWM three-mode cone emission based on Eqs (1–5), and the main results are shown in Fig. 2(b). According to the requirements spatial phase matching conditions discussed in Fig. 2(a), $E_{S3}$ (the outer cones) and $E_{S1}$ (inner cones) propagate along the same direction (the right-hand side ones), and the cones of $E_{S3}$ propagate along the opposite directions respect to $E_{S2}$ and $E_{S1}$ (the left-hand side one).

In light that $E_{S3}$ is set at the place with the highest emission efficiency intentionally ($\Delta k_{S3} = 0$ at $\varphi_{S3} = \varphi_{S2} = 2.9$), we only display the phase mismatching conditions and the normalized generation efficiency of $k_s$ and $k_b$, which are in Fig. 2(c,d), respectively. According to Eqs (4 and 5), we display the phase mismatching $\Delta k_{S3}$ versus transverse coordinates $x$ and $y$ at $z = 10$ m in Fig. 2(c). It is clear to see that $x$ and $y$ located in a circle is corresponding to $\Delta k_{S3,1,3} = 0$, where the six beams are completely phase matching, leading to the largest efficiency to generate the SP-FWMs. However, as $x$ and $y$ deviate the circle, the generation coefficient of the SP-FWMs will reduce greatly.

As shown Fig. 1(b), the two-mode squeezed vacuum states and the generated signals are quantum correlated. As no seeding to those SP-FWM process (both self-diffraction FWM and phase-conjugate FWM), the output states are the two-mode squeezed vacuum states and the generated signals are quantum correlated. However, if only $E_{S1}$ and $E_{S2}$ and considering the dressing effect of $E_{S3}$, the density matrix element for $E_{S1}$ is

$$\rho_{S1}^{(3)} = -\frac{i G G_{S1}^{*} G_{S3}^{*}}{(d_{10} + |G_{12}^{*}| d_{20}) (d_{10}^* + |G_{21}^{*}| d_{20}^*)},$$

where $d_{10} = \Gamma_{02} + i(\Delta_1 + \Delta_3)$, $d_{20} = \Gamma_{02} + (i\Delta_3 + \delta_{13} + \Delta_3)$, $d_{13} = \Gamma_{13} + i(\Delta_3 - \delta_{13} - \Delta_3)$, $d_{30} = \Gamma_{03} + i(\Delta_3 + \delta_{30} + \Delta_3)$, and $\delta_{13}$ is small fluctuation around $\omega_i$ with $|\delta_{13}| \ll \omega_i (i = S_1, A_{S1}, S_2, A_{S2})$. Similar to $\rho_{S1}^{(3)}$, we can obtain the density matrix element for $\rho_{S2}^{(3)}$ via the pathway $\rho_{S2}^{(3)} = \rho_{S1}^{(3)\dagger}$.

$$\rho_{S2}^{(3)} = \frac{-i G G_{S2}^{*} G_{S3}^{*}}{(d_{10} + |G_{12}^{*}| d_{20}) (d_{10}^* + |G_{21}^{*}| d_{20}^*)},$$

where $d_{10} = \Gamma_{02} + i(\Delta_1 - \delta_{13} - \Delta_3)$, $d_{20} = \Gamma_{02} + i(\Delta_3 - \Delta_1)$, and $d_{10}^* = \Gamma_{02} + i(\Delta_1 - \delta_{13} + \Delta_3)$, $d_{20}^* = \Gamma_{02} + i(\Delta_3 + \delta_{13} - \Delta_3)$, and $\delta_{13}$ is small fluctuation around $\omega_i$ with $|\delta_{13}| \ll \omega_i (i = S_1, A_{S1}, S_2, A_{S2})$. Similarly, the density matrix element for $E_{S3}$ can be also obtained via the pathway $\rho_{S0}^{(3)} = \rho_{S1}^{(3)^*}$.

$$\rho_{S3}^{(3)} = \frac{-i G G_{S3}^{*} G_{S1}^{*}}{(d_{10} + |G_{12}^{*}| d_{20}) (d_{10}^* + |G_{21}^{*}| d_{20}^*)},$$

where $d_{10} = \Gamma_{02} + i(\Delta_1 - \delta_{13} + \Delta_3)$, and $d_{20} = \Gamma_{02} + i(\Delta_3 + \delta_{13})$. The measured spots corresponding to SP-SWM, phase-conjugate FWM, self-diffraction FWM are shown in the bottom of Fig. 2(a–c), respectively. When there is no seeding to those SP-FWM process (both self-diffraction FWM and phase-conjugate FWM), the output states are the two-mode squeezed vacuum states and the generated signals are quantum correlated.

Before going to next section, let us pay attention on the comparison between our SP-SWM models and standard FWM scheme. In our theoretical model, SP-SWM process is used to generate quantum correlated triple-mode beams, such process can be considered as the cascading the phase-conjugate FWM and self-diffraction FWM. To be more specific, when pumping fields $E_{S1}$ with intensity $I_{S1}$ is seeded into atomic ensemble and coupled with $|0\rangle \rightarrow |1\rangle$, for a gain $G$ created by $E_{S2}$ twin beams $E_{S1}$ and $E_{S3}$ are simultaneously generated via the self-diffraction FWM process. The intensities of these twin beams $E_{S1}$ and $E_{S3}$ are $I_{S1} = GI_{S1}$ and $I_{S3} = (G - 1)I_{S1}$, respectively.
Although the total power of the twin beams $E_S$ and $E_{AS}$ are significantly amplified, the variance of the relative intensity difference $I_{AS} - I_{AS}$ between them remains unchanged after the amplification. As a result, the relative intensity difference of beams $E_S$ and $E_{AS}$ is squeezed compared with the corresponding shot noise limit (SNL) by an amount of $1/(2G^2 - 1)$. Then, one of the twin beams (say $E_{AS}$, as shown in Fig. 1(b)) is involved in a phase-conjugate FWM, where the output beam $E_S$ is amplified and a conjugate beam ($E_{AS}$) is simultaneously generated for gain $G$ created by $E_S$. The intensities of these two newly generated twin beams ($E_S$ and $E_{AS}$) are $I_{AS} = G^2I_1$ and $I_{AS} = G(G - 1)I_1$, respectively. If one calculates the intensity-difference noise of the three generated beams ($E_{13}$, $E_{STS}$ and $E_{AS}$), given by $I_{AS} = I_{AS} - I_{13}$ and compares it with the corresponding SNL, one will find that the degree of intensity-difference squeezing of the triple beams is given by $1/(2G^2 - 1)$, and the amount of squeezing in our triple-mode case is significantly increased compared with two-mode squeezing. As a matter of fact, the squeezing is generated from internal cascading the self-diffraction and phase-conjugate FWM. Compared with the single self-diffraction or phase-conjugate FWM, the amount of squeezing from SP-SWM is increased from $1/(2G^2 - 1)$ to $1/(2G^2 - 1)$ due to such cascading effect. In other words, by increasing the number of quantum modes, the quantum correlation is also enhanced in our system. Another advantage of our system is the phase insensitivity that makes it possible to easily extend our system to a large number of modes, as it does not require relative phase stability between all the parametric amplification processes.

Multi-Mode Squeezing in Ring Cavity

Now we theoretically study optical squeezing via multi-wave mixing (MWM) process in an atomic ensemble-cavity coupled system. As shown in Fig. 3, here the ring cavity is formed by four mirrors with a longitudinal cavity length $17$ cm. The mirrors $M3$ and $M1$ are input and output mirrors with a radius of $50$ mm, and the reflectance $r3$ ($r1$) and transmittance $t3$ ($t1$) coefficient fulfill the constraint condition ($i = 1, 3$), while $M2$ and $M4$ are highly reflection mirrors. Cavity mode scanning and locking can be implemented by a piezoelectric transducer (PZT) behind $M4$. The length of the atomic vapor cell with the Brewster windows is $L_a = 7$ cm, where the atomic vapor cell is wrapped in $\mu$-metal sheets to shield from external magnetic fields, and a heat tape is placed outside the sheets for controlling the temperature. Since we do not consider Doppler effects in this paper, our analysis is also suitable for standing-wave cavity. For the limit of cavity, the conical emission is disappeared. However, if paired photons or three photons are prepared simultaneously, the squeezing between them still exists. Now, we apply the basic theory to study optical squeezing via MWM process.

The quadrature amplitude summations components and quadrature phase summations components are plotted in Fig. 4 by scanning $\Delta l(\gamma + \gamma_c)$ at different $\Delta l(\gamma + \gamma_c)$, where Fig. 4(a,c,e) are quadrature amplitude summations $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$, $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$, and $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$, and Fig. 4(b,d,f) are the quadrature phase summation $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$, $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$, and $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$, respectively. In Fig. 4, the dotted-line is obtained by blocking the pump fields so as the fifth-order nonlinear process is not active, and the first solid curve in each panel is obtained by injected squeezed vacuum states to cavity and the atomic coupling system, all those (dotted-line and the first solid curve in each panel) can be used as a baseline to examine the effect of the nonlinear process inside cavity on the output states. Compared with the squeezed vacuum states, we can see from Fig. 4(b,c), the variance of quadrature amplitude summation $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$ and quadrature phase summation $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$ are far below the shot-noise limit (SNL) as well as the first solid curve in each panel in a wide frequency range of $\Delta l(\gamma + \gamma_c)$. Therefore, it is enough to assert that $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$ and $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$ further squeezed for the influence of fifth-order nonlinear gain. However, the variance of $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$ and $\hat{\delta}^z\hat{Y}_{13+13}(\Omega)$ becomes noisier than the input squeezed states, as shown in Fig. 4(a,f), for almost all curve are above the SNL. This phenomenon is in line with Heisenberg uncertainty relationship, if the quantum noise variance of quadrature amplitude (Fig. 4(a)) becomes noisier, the variance of quadrature phase (Fig. 4(b)) will be squeezed, and vice versa as shown in Fig. 4(c,f).

On the other hand, we can see from of Fig. 4(a,e) that the evolutions of the quadrature amplitude noise variances $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$ and $\hat{\delta}^+\hat{X}_{13+13}(\Omega)$ show an AT-splitting (the dashed curve). and the noisy degree are amplified, which is different from Fig. 4(e). The main difference can be explained by the interaction Hamiltonian.
describing the SP-SWM process, where the generation of any two photons \( \delta \) and quadrature phase summation \( \hat{c}(t) \) are enhanced for \( \Omega = -20\sim-20(\text{MHz})/(\gamma + \gamma_2) \). From Fig. 5(a1,a2), we can see that only \( \delta \), \( \delta^2 \), and \( \delta^3 \) display the quantum noise variances of the amplitude quadrature summation \( \langle \hat{c}(t)^2 \rangle \), \( \langle \hat{c}(t)^2 \rangle \) and phase quadrature summation \( \langle \hat{c}(t)\hat{c}(t) \rangle \), respectively. The first curve in each case is the result without any dressing fields, and the following five curves from left to right are noise power spectra with \( \Delta_j/(\gamma + \gamma_2) = -20, -10, 0, 10, \) and 20, respectively. The dashed curves are the profiles of noise variances versus \( \Delta_j/(\gamma + \gamma_2) \) with \( \Delta_j/(\gamma + \gamma_2) = 0 \). The dotted lines are the SNL of the corresponding quadrature.

\[ H_1 = i\hbar \kappa S \hat{a}^+_S \hat{a}^+_S \hat{a}^-_S + H.C. \] describing the SP-SWM process, where the generation of any two photons \( \hat{a} \) were accompanied by the annihilation a probe photon \( \hat{a} \). Therefore, in this nonlinear SP-SWM process, \( \hat{a} \) and \( \hat{a} \) have similar quantum characteristics, which is different from \( \hat{a} \). In other words, \( \hat{a} \) and \( \hat{a} \) (\( \hat{a} \)) in competition with each other. Contrary to this, for \( \hat{a} \) and \( \hat{a} \) have similar quantum characteristics, the noisy degree is significantly squeezed for anti-amplification of nonlinear gain. In addition, with the sequential (or nested)-cascade type of double dressing as well as \( \hat{a} \) and \( \hat{a} \) have different quantum characteristics, the tri-peak AT structure of each curve in Fig. 4(a,c) are observed, and the noisy degree of \( \langle \hat{c}^2 \rangle \) and \( \langle \hat{c}^2 \rangle \) are enhanced for amplification of nonlinear gain. These results indicate that the squeezing degree or the noisy degree can be effectively modulated by the nonlinear gain \( \kappa \) as well as the quantum characteristics of the triple-mode.

We now consider the self-diffraction SP-FWM (Fig. 1(b)) process in the ring cavity shown in Fig. 3, where the generated SP-FWM signals \( E_1 \) and \( E_2 \) are propagate along the cavity axis with the same direction forming two cavity modes, and detected by one APD device. As the polarizations of two modes are perpendicular, one can record them independently by putting a polarizer before the APD device and rotating it. On the other hand, in the phase-conjugate SP-FWM process, these two SP-FWM signals will form two modes with different directions, which can be detected by two APD devices. Although the phase-conjugate and self-diffraction SP-FWM are described by different nonlinear coefficient \( \kappa \) and \( \kappa_s \), respectively, these SP-FWM signals (both the phase-conjugate and self-diffraction) have the same quantum characteristics except propagation along different directions. Therefore, the motion equations of such two SP-FWM signals can be written with unified form.

\[
\frac{d\hat{a}_S}{dt} = -i\Delta \hat{a}_S - \gamma \hat{a}_S + \kappa \hat{a}_{AS}^+ + \sqrt{2\gamma} \hat{c}_S + \sqrt{2\gamma} \hat{c}_{AS}^+ \tag{10}
\]

\[
\frac{d\hat{a}_{AS}}{dt} = -i\Delta \hat{a}_{AS} - \gamma \hat{a}_{AS} + \kappa \hat{a}_S^+ + \sqrt{2\gamma} \hat{c}_S + \sqrt{2\gamma} \hat{c}_{AS}^- \tag{11}
\]

where \( \hat{c}_S \) and \( \hat{c}_{AS} \) are the coupled vacuum modes.

Considering the Fourier transform of Eqs (10 and 11) and boundary condition \( \hat{a}_S^+(\Omega) = \sqrt{2\gamma} \hat{a}_S(\Omega) - \hat{a}_{AS}^+(\Omega) \), the quantum noise variance of quadrature amplitude summation \( \langle \hat{c}^2 \hat{X}_{AS}^+ \rangle \) and quadrature phase summation \( \langle \hat{c}^2 \hat{Y}_{AS}^+ \rangle \) at output can be investigated by scanning \( \Delta_j/(\gamma + \gamma_2) \) and \( \Delta_j/(\gamma + \gamma_2) \) simultaneously. To invest noise fluctuation of cavity mode under various injection fields, here EPR field and coherent field is injected into the ring cavity to make a comparison. Firstly, we adopt coherent fields as the injected fields. The quantum noise variances of \( \langle \hat{c}^2 \hat{X}_{AS}^+ \rangle \) and \( \langle \hat{c}^2 \hat{Y}_{AS}^+ \rangle \) are illustrated in Fig. 5(a1,a2), respectively. From Fig. 5(a1,a2), we can see that only \( \langle \hat{c}^2 \hat{X}_{AS}^+ \rangle \) is lower than SNL as \( \Delta_j/(\gamma + \gamma_2) \) scanned from negative to positive, where the maximum squeezing is corresponding to the location of reverse AT splitting created by \( E_2 \), that is, the position of the dark state. While, the quantum noise variances of \( \langle \hat{c}^2 \hat{X}_{AS}^+ \rangle \) become noisier as \( \Delta_j/(\gamma + \gamma_2) \) is scanned in the vicinity of the dressed state. On the other hand, except without considering the dressing effect from \( E_2 \), other conditions in Fig. 5(b1,b2) are same as those in Fig. 5(a1,a2), respectively. In comparison with the cases with and
without dressing effect of $E_0$, the AT splitting in quadrature amplitude and the reverse AT splitting in quadrature phase are disappears, and the location of maximum noisier and squeezing are moved to $\Delta_{y}(\gamma + \gamma_c)$. We can see that the dressed state can effectively control the squeezing process. Therefore, the influence of the AT splitting of $E_c$ on the squeezing is obvious.

Then, by setting $\Delta_{y}(\gamma + \gamma_c) = 15$ (Fig. 6(a1–a2,b1–b2)) and $\Delta_{y}(\gamma + \gamma_c) = 0$ (Fig. 6(c1–c2,d1–d2)), respectively, and scanning $\Delta_{y}(\gamma + \gamma_c)$ as well as $\Delta_{y}(\gamma + \gamma_c)$ synchronously, the suppression and enhancement role of dressed state on the quantum noise variance of $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ and $\langle \delta^2 \hat{Y}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ are studied. In the case of $\Delta_{y}(\gamma + \gamma_c) = 15$, as shown in Fig. 6(a1), the quantum noise variance of $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ becomes noisier and no squeezing when $\Delta_{y}(\gamma + \gamma_c)$ is scanned from positive to negative. Specifically speaking, the noise fluctuation of $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ is significantly enhanced in the region $\Delta_{x} < 0$, and suppressed in the region $\Delta_{x} > 0$, which is corresponding enhancement $(\Delta_{x} = 0, \Delta_{y} = \Delta_{y} = 15)$ conditions of the dressed state, respectively. It should be emphasized that $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ is still no squeezing in suppression region $\Delta_{x} > 0$ for the curve is above the SNL. However, the situation is exactly the opposite in terms of the quadrature phase summation, as shown in Fig. 6(a2), where the profiles of quantum noise variances show that $\langle \delta^2 \hat{Y}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ is squeezed when $\Delta_{y}(\gamma + \gamma_c)$ is scanned, and the degree of squeezing get its maximum in the region $\Delta_{x} < 0$. Fig. 6(b1,b2) are same as those in Fig. 6(a1,a2) except without considering the dressing effect from $E_0$. In comparison the cases with and without $E_0$, the quantum noise variances of the $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ and $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ is unchanged as $\Delta_{y}(\gamma + \gamma_c)$ is scanned. For the case $\Delta_{y}(\gamma + \gamma_c) = 0$, we take the same method to study the influence of dressed state on two-mode squeezing. As shown in Fig. 6(c1,c2), the quantum noise variances of the $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ and $\langle \delta^2 \hat{Y}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ at $\Delta_{y} = 0$ exhibit a pure suppression and a pure enhancement, respectively. It is worth mentioning that the suppression conditions are all $\Delta_{x} = \Delta_{y}$. If the dressing effect of $E_0$ can be neglected, the quantum noise variances are also not affected as shown in Fig. 6(d1,d2). It is clear see that two-mode squeezing can be effectively controlled by the suppression and enhancement of dressed state.

Finally, the influence of dressed state on the squeezing with Einstein-Podolsky-Rosen (EPR) fields injected is shown in Fig. 7(a1–a2), where $\Delta_{y}(\gamma + \gamma_c)$ and $\Delta_{x}(\gamma + \gamma_c)$ are scanned with $\Delta_{y}(\gamma + \gamma_c) = 15$. As shown in Fig. 7(a1), the variance of $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ becomes noisier when $\Delta_{y}(\gamma + \gamma_c)$ is scanned from positive to negative, and the profile of the variances (showing enhancement in $\Delta_{x} < 0$ and suppression in $\Delta_{x} > 0$) is same as the

![Figure 5](image1.png)

**Figure 5.** Theoretically calculated two-mode squeezing based on Eqs (10) and (11) versus $\Delta_{y}(\gamma + \gamma_c)$ and $\Delta_{x}(\gamma + \gamma_c)$, with coherent fields injected, (a1,a2) are $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ and $\langle \delta^2 \hat{Y}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ with the dressing effect of $E_2$, respectively. (b1,b2) are $\langle \delta^2 \hat{X}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ and $\langle \delta^2 \hat{Y}_{\text{AS+S}}^{\alpha}(\Omega) \rangle$ without $E_2$, respectively.

![Figure 6](image2.png)

**Figure 6.** The theoretically calculated squeezing of two-mode versus $\Delta_{y}(\gamma + \gamma_c)$ and $\Delta_{x}(\gamma + \gamma_c)$ synchronously. By setting $\Delta_{y}(\gamma + \gamma_c) = 15$, (a1,a2), (b1,b2) are the amplitude quadrature summation and phase quadrature summation with (without) considering the dressing effect of $E_2$. By setting $\Delta_{y}(\gamma + \gamma_c) = 0$, (c1,c2),(d1,d2) are the amplitude quadrature summation and phase quadrature summation with (without) considering the dressing effect of $E_2$. 

![Image](image3.png)
situation when coherent fields injected is considered. In addition, although \( \langle \hat{a}^\dagger X_{AS+1}^o(\Omega) \rangle \) is injected with squeezed fields and suppressed at \( \Delta_1 > 0 \), there is no squeezing in all region. As mentioned above, for the influence of dressed state as well as injected with squeezed fields, the variance of \( \langle \hat{a}^\dagger Y_{AS+1}^o(\Omega) \rangle \) shown in Fig. 7(a2) is significantly squeezed compared with the injecting coherent fields. To be specific, \( \langle \hat{a}^\dagger Y_{AS+1}^o(\Omega) \rangle \) get its maximum squeezing value at \( \Delta_1 = \Delta_2 = 15 \). On the other hand, the quantum noise variances of \( \langle \hat{a}^\dagger X_{AS+1}^o(\Omega) \rangle \) and \( \langle \hat{a}^\dagger Y_{AS+1}^o(\Omega) \rangle \) do not change versus \( \Delta_1(\gamma + \gamma) \) if the dressing effect from is absent. However, \( \langle \hat{a}^\dagger X_{AS+1}^o(\Omega) \rangle \) and \( \langle \hat{a}^\dagger Y_{AS+1}^o(\Omega) \rangle \) shown in Fig. 7(b1,b2) have a higher squeezing level than those shown in Fig. 6(b1,b2) for injected with squeezed fields. It is worth mentioning that our scheme has following advantages. First, due to the near- and on-resonance nonlinear optical processes can be enhanced by atomic coherence technique, so the generation efficiency of SP-SWM and degree of triple of squeezing (entanglement) can be significantly enhanced by manipulating nonlinear susceptibility and quantum gain. Second, due to electromagnetically induced transparency (EIT) window (MHz), not only the resonance absorption is eliminated, but narrow bandwidth signals at low light level is obtained as well. So compared with correlated photon pairs from SPDC, which have characteristics of very wide bandwidth (THz) and ultra-short coherence time (ps). Our scheme has a narrower-bandwidth (MHz) and longer coherence time (0.1–1.0 μs). Last but not least, the quality of imaging can be well controlled by multiple parameters.

Conclusion

In summary, we have theoretically investigated the multi-mode quantum noise squeezing and amplification with MWM signals in a ring cavity filled with rubidium vapors. It is found that the squeezing and amplification of quantum noise can be effectively modulated by dressed state and nonlinear gain coefficient. Specifically, nonlinear gain leads to the optical squeezing as well as nonlinear AT splitting of cavity mode, and dressed state can be used to reshape the efficiency as well as the location of maximum squeezing point. In optical squeezing, the physical properties of dressed state and nonlinear gain are quite similar. It is worth mentioning that our system has following advantages, first, the amount of squeezing from SP-SWM is significantly improved compared with self-diffraction and phase-conjugate FWM. Second, intensity-difference squeezing from SPDC has the characteristics of very wide bandwidth (THz) and ultra-short coherence time (ps), however, a narrower-bandwidth (MHz) and longer coherence time (0.1–1.0 μs) is implemented from SP-SWM. Such as long coherence time allows us to access and manipulates the spatial squeezing directly. Third, intensity-difference squeezing can be well controlled by multiple parameters. One of the main advantages of our system is that can be directly used in multichannel quantum imaging, and the quality of imaging, including the contrast and resolution, is significantly improved compared with the two-mode squeezing state. The proposed method is also used as implementation of triple-mode entangled source to achieve multi-channel communication.

Theoretical Models

In this part, a new scheme via fifth-order nonlinear channels to produce triple mode squeezed state is proposed as shown in Fig. 3, where \( E_1, E_2 \), and \( E_3 \) are injected into the ring cavity and coupled to \( |0\rangle \to |1\rangle, |1\rangle \to |2\rangle, \) and \( |3\rangle \to |4\rangle \), respectively. Considering the assumption that the fields \( E_2 \) and \( E_3 \) are much larger than the probe \( E_1 \), two SWM (\( E_3 \) and \( E_5 \)) photons are generated, which is accompanied by the annihilation a probe photon \( a_1 \) and three pumping field photon with phase matching condition satisfy \( k_1 = k_3 + k_3 - k_3 - k_3 \) and \( k_5 = k_3 + k_3 - k_3 - k_3 \). In this process, \( E_1, E_3 \) and \( E_5 \) are treated as quantum fields, while \( E_2 \) and \( E_4 \) are considered as classical fields, therefore, the interaction Hamiltonian describing this process can be expressed as

\[
H_I = \hbar \kappa_1 \hat{a}_1 \hat{a}_3 \hat{a}_3^\dagger + \text{H.c.},
\]

where \( \hat{a}_1, \hat{a}_3 \) and \( \hat{a}_3^\dagger \) are the annihilation operator of triple cavity modes \( E_1, E_3 \) and \( E_5 \). The fifth-order nonlinear coefficients \( \kappa \) described by the nonlinear gain in SWM processes, is proportional to \( \rho_{5}^{(2)} \). On the other hand, the Hamiltonian for the probe field is \( H_p = \hbar \kappa_1 \hat{a}_1^\dagger + \text{H.c.} \), where \( \kappa_1 \) is the amplitude of the probe field. Therefore, taking into account the loss, and nonlinear gain, we can obtain the equations for three cavity modes as following:

\[
\frac{d\hat{a}_1}{dt} = -i \Delta \hat{a}_1 - \gamma_1 \hat{a}_1 - \kappa_3 \hat{a}_3 \hat{a}_3^\dagger + \sqrt{2\gamma_1} \hat{a}_1^m + \sqrt{2\gamma_1} \hat{c}_1,
\]

(12)
\[
\frac{d\hat{a}_1}{dt} = -i\Delta \hat{a}_1 - \gamma_1 \hat{a}_1 + \kappa_1 \hat{a}_0^\dagger + \sqrt{2\gamma_1} \hat{a}_1^\dagger + \sqrt{2\gamma_1} \hat{c}_1
\]
(13)
\[
\frac{d\hat{a}_3}{dt} = -i\Delta \hat{a}_3 - \gamma_3 \hat{a}_3 + \kappa_3 \hat{a}_0^\dagger + \sqrt{2\gamma_3} \hat{a}_3^\dagger + \sqrt{2\gamma_3} \hat{c}_3
\]
(14)

where \(\Delta\) is the cavity detuning, \(\hat{a}_0^\dagger, \hat{a}_1^\dagger\) and \(\hat{a}_3^\dagger\) denote the injected fields at \(E_i, E_{1i}\) and \(E_{3i}\) channels, respectively. \(\hat{c}_1, \hat{c}_3\) and \(\hat{c}_\alpha\) are the vacuum modes coupled with the corresponding cavity modes \(\hat{a}_0, \hat{a}_1\) and \(\hat{a}_3\), and \(\gamma_1, \gamma_3\), and \(\gamma_{3i}\) denote the dimensionless damping rate which are related to the amplitude reflection and transmission coefficients of the input and output couplers of the optical cavity.

Without loss of generality, one can decompose the system variables (including the resonant cavity modes, the injected fields, and vacuum modes) into their steady-state values and small fluctuations around the steady-state values, for instance, \(\hat{a}_i = \alpha_i + \delta \hat{a}_i, \hat{a}_0^\dagger = \alpha_{0i}^\dagger + \delta \hat{a}_0^\dagger, \hat{c}_i = \alpha_{ci} + \delta \hat{c}_i\) (\(i = 1, S_1, S_3\)), where \(\alpha_i, \alpha_{0i}^\dagger\) and \(\alpha_{ci}\) indicate the mean values of the corresponding fields, and \(\delta \hat{a}_i, \delta \hat{a}_0^\dagger\) and \(\delta \hat{c}_i\) demonstrate small fluctuations around the steady-state values. The injected probe field is a coherent field, and its fluctuations are the same as the vacuum fluctuations, so \(\alpha_{0i}^\dagger = \varepsilon_i\). However, the generated cavity modes and coupled vacuum modes have zero mean values, i.e., \(\hat{a}_0^\dagger = \delta \hat{a}_0^\dagger\) and \(\hat{c}_i = \delta \hat{c}_i\).

The steady-state solutions can be obtained by letting \(d\alpha_i/dt = 0\) \((i = 1, S_1, S_3)\), and throwing away the vacuum fluctuations as well as the cavity detuning in Eqs (12–14). Therefore, the steady-state value of the triple cavity mode satisfies the following equations

\[
-\gamma_1 \alpha_1 - \kappa_1 \alpha_{3i} \alpha_{S3} + \sqrt{2\gamma_1} \varepsilon_1 = 0,
\]
(15)
\[
-\gamma_1 \alpha_{3i} + \kappa_1 \alpha_1 \alpha_{S3} = 0,
\]
(16)
\[
-\gamma_3 \alpha_{3i} + \kappa_3 \alpha_1 \alpha_{S3} = 0.
\]
(17)

In order to simplify the calculation, we assume that \(\hat{a}_0\), \(\hat{a}_1\), and \(\hat{a}_3\) are nearly frequency degenerate, leading damping rates to be identical \((\gamma_1 = \gamma_{3i} = \gamma_{3})\). Now, the steady-state values of of triple cavity modes have following value:

\[
\alpha_1 = \frac{\gamma_1}{\kappa_S},
\]
(18)
\[
\alpha_{3i} = \alpha_{S3} = \pm \sqrt{\frac{2\gamma_1 \varepsilon_1 \kappa_S - \gamma_1^2}{\kappa_S^2}}.
\]
(19)

By means of linearized analysis procedure, small fluctuations around of triple cavity mode can be obtained,

\[
\frac{d\delta \hat{a}_1}{dt} = -i\Delta \delta \hat{a}_1 - \gamma_1 \delta \hat{a}_1 - \kappa_1 (\alpha_{3i} \delta \hat{a}_{S1} + \kappa_{3i} \delta \hat{a}_{S3}) + \sqrt{2\gamma_1} \delta \hat{a}_1^\dagger + \sqrt{2\gamma_1} \delta \hat{c}_1
\]
(20)
\[
\frac{d\delta \hat{a}_3}{dt} = -i\Delta \delta \hat{a}_3 - \gamma_3 \delta \hat{a}_3 - \kappa_3 (\alpha_{3i} \delta \hat{a}_{S1} + \kappa_{3i} \delta \hat{a}_{S3}) + \sqrt{2\gamma_3} \delta \hat{a}_3^\dagger + \sqrt{2\gamma_3} \delta \hat{c}_3
\]
(21)
\[
\frac{d\delta \hat{c}_3}{dt} = -i\Delta \delta \hat{c}_3 - \gamma_3 \delta \hat{c}_3 - \kappa_3 (\alpha_{3i} \delta \hat{a}_{S1} + \kappa_{3i} \delta \hat{a}_{S3}) + \sqrt{2\gamma_3} \delta \hat{c}_3^\dagger + \sqrt{2\gamma_3} \delta \hat{c}_{S3}
\]
(22)

Now, we need the fluctuations of quadrature amplitude \((\hat{X}_i = \hat{a}_i + \hat{a}_i^\dagger)\) and quadrature phase \((\hat{Y}_i = -i(\hat{a}_i - \hat{a}_i^\dagger))\) components to study squeezing characteristics between triple modes. Considering the Fourier transform of the operators, Eqs (20–22) can be recasted in terms of the quadrature amplitude and phase operators:

\[
\Delta \delta \hat{X}_1 - (\gamma_1 + \kappa_1) \delta \hat{X}_1 - \kappa_1 [\alpha_{3i} \delta \hat{X}_{S1} + \alpha_{3} \delta \hat{X}_{S3}] + \sqrt{2\gamma_1} \delta \hat{X}_1^\dagger + \sqrt{2\gamma_1} \delta \hat{X}_{c1} = 0,
\]
(23)
\[
-\Delta \delta \hat{X}_1 - (\gamma_1 + \kappa_1) \delta \hat{X}_1 - \kappa_1 [\alpha_{3i} \delta \hat{Y}_{S1} + \alpha_{3} \delta \hat{Y}_{S3}] + \sqrt{2\gamma_1} \delta \hat{Y}_1^\dagger + \sqrt{2\gamma_1} \delta \hat{Y}_{c1} = 0,
\]
(24)
\[
\Delta \delta \hat{Y}_{S1} - (\gamma_1 + \kappa_1) \delta \hat{Y}_{S1} - \kappa_1 [\alpha_{3i} \delta \hat{X}_1 + \alpha_{3} \delta \hat{X}_{S3}] + \sqrt{2\gamma_1} \delta \hat{Y}_{S1}^\dagger + \sqrt{2\gamma_1} \delta \hat{Y}_{c1} = 0,
\]
(25)
\[
-\Delta \delta \hat{Y}_{S1} - (\gamma_1 + \kappa_1) \delta \hat{Y}_{S1} - \kappa_1 [\alpha_{3i} \delta \hat{Y}_{S1} + \alpha_{3} \delta \hat{Y}_{S3}] + \sqrt{2\gamma_1} \delta \hat{Y}_{S1}^\dagger + \sqrt{2\gamma_1} \delta \hat{Y}_{c1} = 0,
\]
(26)
\[ \Delta \delta \hat{Y}_{SS} - (\gamma_1 + \delta \Omega) \delta \hat{X}_{SS} + \kappa_3 [\alpha_3 \delta \hat{X}_1 + \alpha_1 \delta \hat{X}_{33}] + \sqrt{2 \gamma_1} \delta \hat{Y}_{SS} + \sqrt{2 \gamma_1} \delta \hat{X}_{33} = 0, \]

(27)

\[ -\Delta \delta \hat{X}_{33} - (\gamma_1 + \delta \Omega) \delta \hat{Y}_{33} + \kappa_3 [\alpha_3 \delta \hat{Y}_1 - \alpha_1 \delta \hat{Y}_{33}] + \sqrt{2 \gamma_1} \delta \hat{Y}_{SS} + \sqrt{2 \gamma_1} \delta \hat{Y}_{33} = 0, \]

(28)

where \( \Omega \) is the analysis frequency. Now, these equations can be solved in the frequency domain under the boundary condition \( \hat{a}^{\text{out}}(\Omega) = \sqrt{2 \gamma_1} \hat{a}_1(\Omega) - \hat{a}_3(\Omega) \), and the spectra of squeezing characteristics between triple modes in terms of the input fluctuation can be obtained analytically. What's more, the fluctuations of quadrature amplitude summation is same as the quadrature phase difference of any two output modes, and the quadrature amplitude difference is same as the quadrature phase summation of any two output modes, therefore, we will investigate the triple modes squeezing by means of amplitude and quadrature phase summation.

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Author Contributions

F.W. wrote the main manuscript and contributed to experimental analysis. H.W. and Y.Z. provided the idea. Z.L., Y.Z., H.G., J.C. and H.A. contributed to the presentation and execution of the theoretical work. All authors discussed the results and contributed to the writing of the manuscript.

Additional Information

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