Research Article

Analysis of Fission Products’ Release in Pebble-Bed High-Temperature Gas-Cooled Reactor Fuel Elements Using a Modified FRESCO II Numerical Model

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The radiation safety design and emergency analysis of an advanced nuclear system highly depend on the source term analysis. In modular high-temperature gas-cooled reactors (HTGRs), the release rates of fission products (FPs) from fuel elements are the key issue of source term analysis. The FRESCO-II code has been established as a useful tool to simulate the accumulation and transport behaviors of FPs for many years. However, it has been found that the mathematical method of this code is not comprehensive, resulting in large errors for short-lived nuclides and large time step during calculations. In this study, we used the original model of TRISO particles and spherical fuel elements and provided a new method to amend the FRESCO-II code. The results show that, for long-lived radionuclides (Cs-137), the two methods are perfectly consistent with each other, while in the case of short-lived radionuclides (Cs-138), the difference can be more than 1%. Furthermore, the matrix method is used to solve the final release rates of FPs from fuel elements. The improved analysis code can also be applied to the source term analysis of other HTGRs.

1. Introduction

Modular high-temperature gas-cooled reactors (HTGRs) are generally considered to have the technical characteristics of a Generation IV (Gen-IV) nuclear energy system [1]. When analyzing the emergency action and safety principles of an HTGR, it is crucial to know the source term under normal and accident conditions. Source term analysis could provide the generation, quantity, release, and radiation hazard of radionuclides in a nuclear power plant. Owing to the use of high performance fuel elements and TRISO particles, the fission products (FPs) can be effectively retained in the reactor core [2]. However, after decades of operation of the reactor, many FPs may escape from the fuel elements (with a lifetime of approximately 3 years) through permeation and diffusion effects, which has contributed to the main source of radioactivity in the primary circuit and other parts of the nuclear power plant [3, 4].

In order to calculate the amount of FPs in the primary circuit, the numerical simulation code FRESCO-II was developed at Forschungszentrum Jülich in Germany in the early 1980s by Krohn and Finken [5]. This code has been used for decades in HTGRs at Germany, China, and other countries; the results have been compared in many benchmark calculations and have been validated through experiments [6]. Based on the FRESCO-II code and other codes (FRESCO-I, PANAMA, SPATRA, and so on), the uniform and integrated code package STACY (Source Term Analysis Code System) was developed by Allelein et al. in 2010 [7]. Recently, the new simulation package FRAT for prediction and evaluation of full core fission product release was developed by Li et al. at Tsinghua University (China) [8].

All of these simulation codes are based on Fick’s law of diffusion [9, 10], and the results are obtained based on different discrete methods and numerical simulation processes. After using the original model and method of the
FRESCO-II code, it has been found that there is a small error in the expression of the process coefficient. Consequently, the model is non-physical when considering nuclide decay terms, resulting in large errors for short-lived nuclides and large time steps. In this study, all coefficients were strictly derived on the basis of the modified model. Additionally, the simulation results of the new and old models are compared herein.

### 2. Features of HTGR Fuel

The fuel element used in a HTGR is coated spherical fuel particles with a graphite substrate [11]. The research and design of coated fuel particles have gone through two stages. In the initial design, the coated fuel particle structure is of B-isotropic (BISO) type, i.e., a loose and a dense pyrolytic carbon layer on the outer coating of the active core. However, after many irradiation experiments and safety tests, the BISO fuel particle gradually exposed its structural shortcomings; these were mainly reflected in the high level of heavy metal contamination during the coating deposition and the low retention ability for certain metal FPs (such as strontium). Based on the BISO fuel particle, the tri-isotropic (TRISO) fuel particle is designed. The main advantage of TRISO fuel particles is their excellent retention ability for various radioactive FPs. Experiments have shown that the integrity of the TRISO structure can be maintained at temperatures below 1600°C.

Considering a pebble-bed modular HTGR as an example, a spherical fuel element with a diameter of 60 mm was used (shown in Figure 1). Each fuel element contains approximately 12,000 TRISO fuel particles consisting of five parts: (1) an enriched UO$_2$ kernel surrounded by subsequent layers, (2) a loose pyrolytic carbon (buffer) layer, (3) an inner pyrolytic carbon (PyC) layer, (4) silicon carbide (SiC), and finally, (5) an outer pyrocarbon (OPyC) layer [11].

### 3. Transport Model of FPs

The main transport process of FPs in the fuel elements is their diffusion in various materials (shown in Figure 2) [9]. For intact TRISO fuel particles, FPs must diffuse through all coating layers and then through the graphite matrix before entering the coolant. For the failure particles, the FPs can enter the graphite matrix directly. In addition, the FPs produced by uranium contamination in graphite grains are considered to be the same as failure particles.

If the fuel element, TRISO particles, and graphite grains are regarded as uniform spheres, the diffusion of FPs in these media can be described by the same equation. According to Fick’s diffusion law, the release fractions of FPs from the spherical fuel elements can be calculated using the following diffusion equation [12]:

$$\frac{\partial C}{\partial t} = D(T) \left( \frac{\partial^2 C}{\partial r^2} + \frac{2}{r} \frac{\partial C}{\partial r} \right) + Q - \lambda C,$$

where $C$ is the FP concentration in the diffusion medium (in atoms/cm$^3$) and can be obtained from the inventory, $t$ is the time (in s), $r$ is the spatial coordinate (in cm), $Q$ is the production rate of FPs (in atom/cm$^3$·s), $\lambda$ is the decay constant of nuclide (in s$^{-1}$), and $D(T)$ is the diffusion coefficient (in cm$^2$/s) depending on temperature $T$ (in K) and activation energy $E$ (in J/mol) given by the following equation:

$$D(T) = D_0 \cdot \exp\left( -\frac{E}{R \cdot T} \right),$$

where $R$ is the ideal gas constant ($R = 8.3143$ J/(mol·K)) and $D_0$ is the diffusion frequency factor (in cm$^2$/s). The corresponding boundary condition can be expressed as

$$-D \frac{\partial C}{\partial r} \bigg|_{r=r_p} = \beta (C_{rp} - C_{gr}),$$

where $\beta$ is the interface diffusion between different materials, $C_{rp}$ is the concentration of FPs on the surface of the fuel element, and $C_{gr}$ is the average concentration of FPs in the helium outside the fuel element.

### 4. Numerical Simulation

Theoretically, the concentration at any time and position can be obtained by solving equations (1)–(3). However, the
explicit expression of $C(r,t)$ is usually very complex and difficult to solve [13].

To address this challenge, the numerical simulation method is used in the FRESCO-II code and other related codes [14]. In this method, the whole sphere is divided into $N$ thin layers of spherical shell with a volume of $V_i$ ($i = 1, 2, ..., N$) (presented in Figure 3(a)).

Considering that the concentration at the $i$th spherical shell is $C_i$ and assuming that the concentration is a linear function of radius $r$, the concentration between two adjacent spherical shells can be expressed as follows (shown in Figure 3(b)):

$$c = C_i + \frac{C_{i+1} - C_i}{r_{i+1} - r_i} (r - r_i).$$  \hspace{1cm} (4)

In particular, assuming that the concentration distribution is a quadratic curve for the central sphere because the concentration gradient is zero at the central point, the concentration can be derived as follows:

$$c = C_N - 2 \frac{C_{N/2} - C_N}{r_N} (r - r_N) - \frac{C_{N/2} - C_N}{r_N}(r - r_N)^2.$$  \hspace{1cm} (5)

where $C_{N/2}$ represents the concentration at the central point. For the $i$th spherical shell, the mass conservation equation is as follows:

$$\frac{d}{dt} \int_{V_i} c \cdot dV = Q \cdot V_i - \lambda \int_{V_i} c \cdot dV - J_i \cdot F_i + J_{i+1} \cdot F_{i+1},$$  \hspace{1cm} (6)

where the left side of this equation represents the concentration change during $dt$ time. The right side represents the various sources of concentration change, i.e., the generation of fission with rate $Q$, the disappearance of decay, and the diffusion from the inner layer into the target layer and from the target layer into the outer layer, respectively. According to Fick’s first diffusion law, the diffusion rate per unit area $J$ can be expressed as

$$J_i = -D_i \frac{C_{i+1} - C_i}{r_{i+1} - r_i} \quad (i \neq N),$$

$$J_N = -2D_i \frac{C_{N/2} - C_N}{r_{N/2} - r_N}, \quad (i = N).$$  \hspace{1cm} (7)

Then, we can discretize the mass conservation equation (6) using the average change rates instead of instantaneous change rates. For the left side of equation (6), it can be approximated by replacing $dt$ with $\Delta t$ as follows:

$$\frac{d}{dt} \int_{V_i} c \cdot dV = \frac{1}{\Delta t} \left[ \int_{V_i} c^{k+1} \cdot dV - \int_{V_i} c^k \cdot dV \right],$$  \hspace{1cm} (8)

where the superscript index $k$ represents the time step; a larger value corresponds to a later time point.

It should be emphasized that, until this step, all the symbols and equations are the same as the ones in FRESCO-II code. However, the next derivation proposes amendments to the FRESCO-II code for the right side of equation (6). In the FRESCO-II code, the concentration appearing on the right side is set to be a future time value, i.e., the top index is $k + 1$. Obviously, this assumption is nonphysical because the concentrations in each spherical shell are all changing dynamically. Therefore, a new method is proposed through using the time average concentrations instead of future time concentrations; this is also consistent with the treatment of the left side of equation (6). Then, the expression is derived as follows:

$$Q \cdot V_i - \lambda \int_{V_i} c \cdot dV - J_i \cdot F_i + J_{i+1} \cdot F_{i+1}$$

$$= Q \cdot V_i - \frac{\lambda}{2} \left( \int_{V_i} c^{k+1} \cdot dV + \int_{V_i} c^k \cdot dV \right)$$

$$- \frac{1}{2} \left( f^{k+1}_i + f^k_i \right) \cdot F_i + \frac{1}{2} \left( f^{k+1}_{i+1} + f^k_{i+1} \right) \cdot F_{i+1}.$$  \hspace{1cm} (9)

From the combination of equations (6)–(9), the new equation can be reorganized as

$$a_{i+1}c_i^{k+1} + b_{i+1}c_{i+1}^{k+1} + d_{i+1}^{k+1}c_{i+1} = e_{i+1}, \quad (i = 1, 2, 3, ..., N - 1).$$  \hspace{1cm} (10)

The coefficients are given as follows:

$$a_{i+1} = y_i \left( 1 + \frac{1}{2} \lambda \Delta t \right) + \frac{1}{2} \frac{F_i}{V_i} \frac{\Delta t}{r_{i+1} - r_i},$$  \hspace{1cm} (11)

$$b_{i+1} = (1 - y_i) \times \left( 1 + \frac{1}{2} \lambda \Delta t \right) - \frac{1}{2} \frac{F_i}{V_i} \frac{\Delta t}{r_{i+1} - r_i},$$

$$- \frac{1}{2} \frac{F_{i+1}}{V_i} \frac{\Delta t}{r_{i+1} - r_{i+1}},$$  \hspace{1cm} (12)

$$d_{i+1} = \frac{1}{2} \frac{F_{i+1}}{V_i} \frac{\Delta t}{r_{i+1} - r_{i+1}},$$  \hspace{1cm} (13)

$$e_{i+1} = \left[ y_i \left( 1 + \frac{1}{2} \lambda \Delta t \right) - \frac{1}{2} \frac{F_i}{V_i} \frac{\Delta t}{r_{i+1} - r_i} \right] c_i^k$$

$$+ \left( (1 - y_i) \left( 1 - \frac{1}{2} \lambda \Delta t \right) + \frac{1}{2} \frac{F_i}{V_i} \frac{\Delta t}{r_{i+1} - r_i} \right)$$

$$+ \frac{1}{2} \frac{F_{i+1}}{V_i} \frac{\Delta t}{r_{i+1} - r_{i+1}}$$

$$\cdot (1 - y_i) c_{i+1}^{k+1} - \frac{1}{2} \frac{F_{i+1}}{V_i} \frac{\Delta t}{r_{i+1} - r_{i+1}} c_{i+2}^{k+1} + Q \Delta t,$$  \hspace{1cm} (14)

$$y_i = 1 - \frac{3}{r_{i+1}^3 - r_i^3} - \frac{1}{r_{i+1}^3 - r_i^3} \left[ \frac{r_{i+1}^4 - r_i^4}{4} - \frac{r_{i+1}^3 r_i - r_i^3}{3} \right].$$  \hspace{1cm} (15)

Notably, equation (15) must be identical to that in the FRESCO-II code; nevertheless, the incorrect subscript index $i-1$ of the radius cubic in the rightmost fraction appeared in the FRESCO-II code.

The two boundary conditions for the outermost shell contact with the environment and the central shell can be expressed as follows:
-D_{r1} \frac{c_{k+1}^1}{r_2 - r_1} = \beta (c_1^k - c_{env})

\Rightarrow \left( \beta - \frac{D_1}{r_2 - r_1} \right) c_{k+1}^1 + D_1 \cdot \frac{1}{r_2 - r_1} \cdot c_{k+2}^1

\Rightarrow b_1 c_{k+1}^1 + d_1 c_{k+2}^1 = e_1,

a_{N+1} = y_N \left( 1 + \frac{1}{2} \lambda \Delta t \right) + \frac{1}{2} D_N \frac{F_N}{v_N} \cdot \frac{2M}{r_N}

b_{N+1} = (1 - y_N) \left( 1 + \frac{1}{2} \lambda \Delta t \right) - \frac{1}{2} D_N \frac{F_N}{v_N}

d_{N+1} = 0,

e_{N+1} = \left[ y_N \left( 1 - \frac{1}{2} \lambda \Delta t \right) - \frac{1}{2} D_N \frac{F_N}{v_N} \cdot \frac{2M}{r_N} \right] c_{k+1}^1

+ \left[ (1 - y_N) \left( 1 - \frac{1}{2} \lambda \Delta t \right) + \frac{1}{2} D_N \frac{F_N}{v_N} \cdot \frac{2M}{r_N} \right] c_{k+1}^1

+ Q_N \Delta t,

y_N = 0.6. \quad (16)

Equation (10) is a recurrence relation for both time and space dimensions and can be further represented in the matrix form as follows:

$$\mathbf{M} \cdot \mathbf{c}^{k+1} = \mathbf{E}^k,$$  \quad (17)

where $\mathbf{M}$ is full rank. Furthermore, the elements of the matrix $\mathbf{M}$ are all time independent, i.e., they are only related to the space index and can be determined by geometric parameters. The vector $\mathbf{E}^k$ is a function of the space index and the concentrations in past time points. The unknown vector $\mathbf{c}^{k+1}$ is our target concentration in the future time point, which can be obtained by solving the matrix equation (17) as follows:

$$\mathbf{c}^{k+1} = \mathbf{M}^{-1} \cdot \mathbf{E}^k. \quad (21)

This equation indicates that any concentrations in any future time point can be recursively solved when an initial concentration state is given.
Table 3: Comparison of two methods for Cs-137 fractional release rates from a pebble.

| Temperature (°C) | 600    | 700    | 800    | 900    | 1000   | 1100   | 1200   | 1300   | 1400   | 1500   | 1600   |
|------------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| FRESCO-II (s⁻¹)  | 3.9192E−16 | 1.7100E−15 | 6.5096E−14 | 6.3373E−13 | 2.4107E−12 | 2.3764E−10 | 1.5134E−09 | 3.9838E−09 | 7.1964E−09 | 9.7246E−09 | 1.0717E−08 |
| FERRA (s⁻¹)      | 3.9198E−16 | 1.7096E−15 | 6.5130E−14 | 6.3414E−13 | 2.3990E−12 | 2.3774E−10 | 1.5145E−09 | 3.9864E−09 | 7.2005E−09 | 9.7284E−09 | 1.0718E−08 |
| Ratio            | 0.9998  | 1.0002 | 0.9995 | 0.9994 | 1.0049 | 0.9996 | 0.9993 | 0.9993 | 0.9994 | 0.9996 | 0.9999 |
Table 4: Comparison of two methods for Cs-138 fractional release rates from a pebble.

| Temperature (°C) | 600   | 700   | 800   | 900   | 1000  | 1100  | 1200  | 1300  | 1400  | 1500  | 1600  |
|------------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| FRESCO-II (s⁻¹)  | $1.6609E-15$ | $2.1412E-14$ | $1.6480E-13$ | $7.8264E-13$ | $2.3831E-12$ | $5.3521E-12$ | $1.0020E-11$ | $1.6930E-11$ | $3.1376E-11$ | $8.9169E-11$ | $3.0714E-10$ |
| FERRA (s⁻¹)      | $1.6609E-15$ | $2.1412E-14$ | $1.6480E-13$ | $7.8264E-13$ | $2.3831E-12$ | $5.3521E-12$ | $1.0027E-11$ | $1.7014E-11$ | $3.1707E-11$ | $8.9918E-11$ | $3.0952E-10$ |
| Ratio            | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 0.9993 | 0.9951 | 0.9896 | 0.9917 | 0.9923 |
5. Results and Discussion

The numerical simulation method introduced in Section 4 has been implemented in Python and is named Fuel Element Release Rate Analysis (FERRA) Code. Considering the HTR-PM (high-temperature gas-cooled reactor-pebble bed modules) fuel element as an example, a series of comparative calculations are performed in this study. The main parameters of the HTR-PM are listed in Table 1 [2].

The kernel and the four-layer coating materials are separated into 39 thin spherical shells in both the FRESCO-II and FERRA codes. Two cesium isotopes, Cs-137 and Cs-138 (with a decay constant of approximately $7.3 \times 10^{-10}$ s$^{-1}$ and $3.6 \times 0.04$ s$^{-1}$, respectively), were used as an example to compare the differences between the results of the two methods. The diffusion coefficients of Cs in each material are listed in Table 2 [11].

Based on these parameters, after a 25,400 h burn-up (3 years average life time of fuel element), the fractional release rates of Cs-137 and Cs-138 from a pebble over the temperature range from 600°C to 1600°C are calculated and presented in Tables 3 and 4.

The results show that, for the long-lived radionuclide Cs-137, the two methods are perfectly consistent with each other at all temperatures with an error less than 1%. However, the case for the short-lived radionuclide Cs-138 is slightly different. A maximum of more than 1% error occurred when the temperature was higher than 1200°C. Furthermore, the release rates are overall underestimated in the FRESCO-II code; this can be attributed to the underestimation of the interlayer transport rates.

6. Conclusions

Thus far, the FRESCO-II code and its successor provided powerful simulation tools for handling the FP release rates in HTGR. Based on reliable release rates, the source term analysis could be credible and safety design and emergency evaluation could be performed.

In order to improve the reliability of the source term analysis codes, we used the original model and derivation process of the FRESCO-II code. An index error has been identified, and a new treatment for transport rates is proposed. After the code implementation, the new simulation code FERRA is developed, and a series of tests are performed. The results show that the FRESCO-II and FERRA codes are perfectly consistent with each other for both long-lived and short-lived radionuclides. Another valuable finding is that the release rates are overall underestimated in the FRESCO-II code, which suggests that the FERRA results are more conservative. As a conclusion, continuous improvements to computing tools can make a great contribution to the design of pebble-bed HTGRs.

Data Availability

All the data used to support the findings of the study are obtained from open source literatures and all the references cited within the article.

Disclosure

The contents of this manuscript are not now under consideration for publication elsewhere.

Conflicts of Interest

The authors declare that they have no conflicts of interest.

Authors’ Contributions

All authors of this manuscript have directly participated in planning, execution, and/or analysis of this study.

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