Joint Coherent and Non-Coherent Detection and Decoding Techniques for Heterogeneous Networks

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Abstract—Cellular networks that are traditionally designed for human-type communication (HTC) have the potential to provide cost-effective connectivity to machine-type communication (MTC). However, MTC is characterized by unprecedented traffic in cellular networks, thus posing a challenge to its successful incorporation. In this work, we propose a unified framework for amicable coexistence of MTC and HTC. We consider a heterogeneous network where machine-type devices coexist with enhanced mobile broadband (eMBB) devices and propose transceiver techniques that promote efficient signal recovery from these devices. For this, we present an eMBB pilot and MTC data generation strategy that facilitates joint coherent decoding of eMBB data and non-coherent decoding of MTC data. Furthermore, we assess the feasibility of coexistence using receiver operating characteristics, outage probability, and normalized mean square error (NMSE). Our numerical results reveal that a harmonious coexistence of the heterogeneous services can be achieved with properly configured average signal-to-noise ratios and pilot length.

Index Terms—Coherent and non-coherent decoding, detection, enhanced mobile broadband, grant-free, machine-type communication, sparse signal recovery.

I. INTRODUCTION

MACHINE-type communication (MTC) is of paramount importance in the realization of a digitally connected society due to its application in cellular Internet of Things (IoT) [1], [2], [3]. As a result, there is an accelerated deployment of machine-type devices (MTDs) that perform tasks such as health, pollution, energy consumption, and infrastructure monitoring [4], [5]. To provide cost-effective connectivity to these devices, it is advantageous to utilize existing cellular networks [6], [7]. However, cellular connectivity is traditionally designed for human-type communication (HTC) so that the key differences hinder seamless HTC/MTC integration. For instance, contrary to HTC, MTC is characterized by sporadic uplink traffic of short packets [2]. Furthermore, the massive number of MTDs in a cell makes it infeasible to allocate orthogonal pilot sequences, thus, challenging conventional multiple access transceiver techniques [8], [9].

To handle MTC’s sporadic traffic and massiveness of MTDs, grant-free non-orthogonal multiple access (GF-NOMA) techniques have been proposed [10], [11]. These techniques allow the MTDs to transmit without waiting for a permission, which is conventionally granted through a handshaking process [8]. However, collisions become unavoidable, thus, potentially degrading the system performance. To resolve the collisions, several signal detection algorithms which exploit the sporadic traffic of MTDs have recently been proposed [8], [9], [12], [13], [14]. In essence, the received signal is a compressed measurement of sparse (effective) channels for different users, while the base station (BS) is tasked with identifying and estimating these channels. This two-fold inference task involving sparse signal recovery in MTC gives rise to the problem of compressed sensing based multi-user detection (CS-MUD), which can be formulated and solved using compressed sensing theory [15], [16], [17]. Specifically, CS-MUD problems can be posed as coherent or non-coherent signal recovery problems [18], [19]. Coherent recovery uses channel state information (CSI), hence, it is only efficient in scenarios where the payload is much greater than the metadata [20], [21]. On the other hand, non-coherent recovery is carried out without CSI and it is only favorable for short packet data traffic [22], [23], [24], [25].

From the preceding discussions, it is apparent that GF-NOMA suited for MTDs differs from grant based medium access techniques used for HTC [26]. Fundamentally, GF-NOMA reduces the access latency at the cost of increasing collisions, while the opposite is true for grant based medium access. In addition, while coherent decoding techniques are suitable for eMBB transmissions, non-coherent decoding techniques are specifically well suited for MTC. In spite of these differences, a 5G and beyond (5GB) cellular network must accommodate both eMBB and MTC using limited resources [27]. It is therefore important to note that joint coherent decoding of eMBB devices and non-coherent detection of MTDs has great potential to alleviate the spectrum

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scarcity problem by promoting harmonious coexistence of the different services. To this end, the main focus of our paper is to introduce a framework for coexistence of MTC and HTC services (i.e., eMBB) within the same spectrum resource block. We subsequently present a brief literature review of some of the works that gave us the impetus to pursue this work.

A. Related Literature

Sparse signal recovery (SSR) algorithms have for long been applicable in signal processing frameworks, where signals have sparse representations in a certain basis [16], [28]. In light of this, the data traffic from MTDs can be captured using sparse representations. Furthermore, the number of MTDs is expected to grow to around $10^6$ devices per cell in the next few years, among which only a limited set will concurrently be active [29]. From the receiver perspectives, further deployments of MTDs result in a complex SSR problem, which may cause performance degradation. Owing to this, there is an increased research interest in CS-MUD [30], [31].

Among some of the markedly proposed solutions to CS-MUD problems are graphical models due to their ability to represent complex information using probability distributions [32], [33]. Based on this property, message passing (MP) algorithms on graphical models have been extensively used to handle the sporadic traffic from MTDs, e.g., using belief propagation (BP) [34], approximate MP (AMP) [21], [35], [36], [37], [38], and expectation propagation (EP) [20].

We et al. [21] proposed a novel minimum mean square error (MMSE) denoiser for AMP in massive deployments of MTDs. Their work showed that it is possible to drive both the probability of miss detection and the probability of false alarm to zero in massive multiple-input multiple-output (MIMO) setups. Their algorithm is designed for coherent detection, hence does not exploit the short packet structure of MTDs. Senel et al. [8] introduced a non-coherent AMP algorithm that uses a likelihood ratio of the information symbols. Different from [8], where the assumed prior distributions do not take activity pattern of MTDs into consideration, Tang et al. proposed a Bayes optimal algorithm in [39]. Rodrigo et al. [29] analyzed a new dimension to device activity detection by considering asynchronous device activity in a given coherence interval. Another perspective of MP is seen in [20], where Ahn et al. proposed a joint user activity detection and channel estimation algorithm based on EP. In spite of its ability to handle any activity pattern, a key limitation lies in the assumption of a single-antenna BS scenario, which is not practical for supporting massive connectivity. Huang et al. [14] proposed generalised AMP and deep learning based non-coherent detection algorithms for scenarios subject to Rician fading, where the activity pattern differs from one MTD to another. Furthermore, Huang et al. [40] proposed a data-driven non-coherent transceiver techniques for short packet transmissions. Apart from MP based approaches, other solutions to CS-MUD problem exploit convex optimization techniques. To this end, Chen et al. [22] proposed a covariance aided non-coherent detection algorithm, and Djelouat et al. [40] proposed a joint user identification and channel estimation algorithm using alternating direction method of multipliers (ADMM).

One shortcoming of the previous works is the assumption that MTDs operate alone in the corresponding resource block. This may disable their application to 5GB cellular networks where heterogeneous services, i.e., ultra-reliable low latency communication (URLLC), MTC, and eMBB may need to coexist amicably [11], [27], [41], [42]. As previously mentioned, existing HTC cellular networks are appealing for providing connectivity to MTC. However, successful incorporation of MTC into cellular networks designed for HTC requires tailoring algorithms that enable i) resolution of multiple access interference and collisions of MTDs, ii) efficient short packet data transmissions, and iii) coexistence of MTC with other services.

In our previous work [43], we proposed a pilot design strategy that enables efficient channel estimation of a single eMBB device in the presence of MTC. In addition, we presented a joint detection of MTDs with successive interference cancellation (SIC) of eMBB data. In this regard, [43] was a first necessary step for enabling MTC-eMBB coexistence by studying the single eMBB user scenario and the first phase of the transmission block, i.e., metadata/pilot training phase. We had assumed that the interference power on the detection process of MTDs emanated exclusively from the receiver noise and the channel estimation error of the eMBB device. Meanwhile, in this paper, we advance the state-of-the-art by considering a more general multi-eMBB user setup and the entire transmission block, i.e., metadata and data decoding. Under this setup, signals cannot be guaranteed to be orthogonal to each other in the second transmission block. This results in stronger interference and thus, the present work provides a more practical coexistence solution for the eMBB and MTC services. To the best of our knowledge, this is the first work that presents a unified framework to accommodate joint coherent and non-coherent signal reception in a heterogeneous 5GB network consisting of eMBB and MTC traffic.

B. Contributions

We consider a heterogeneous network, where eMBB devices and MTDs are co-hosted in the same spectrum resource block. By acknowledging that the two services have heterogeneous requirements and characteristics, we propose service-specific techniques: coherent decoding for eMBB devices and non-coherent decoding for MTDs. Coherent decoding is facilitated by properly designed pilot symbols for eMBB devices, while non-coherent decoding is achieved by an optimized message generation strategy for MTDs. Furthermore, we consider joint activity and data decoding (JADD) of MTDs as a CS-MUD problem. This CS-MUD problem is more challenging than those in, e.g., [20], [21], [40], due to possible interference from eMBB signals.

The key contributions of our paper are:

- We propose novel transceiver signal processing techniques that facilitate the joint detection/decoding of eMBB and MTC data within the same spectrum resource block. This facilitates coexistence of heterogeneous services, thus, addressing a practical need for 5GB cellular connectivity.
• We propose a novel message generation strategy for MTDs. The generated messages are the transmitted symbols from MTDs and also used as a measurement (or sensing) matrix in compressed sensing terminology [16]. This matrix is designed such that part of its structure maintains orthogonality with the pilot sequences of the eMBB devices. The orthogonality makes it possible to get interference-free channel estimates, which leads to more efficient coherent decoding and SIC.

• We adapt state-of-the-art MTC detection algorithms to the considered heterogeneous scenario. Specifically, AMP [8], [21], ℓ_{2,1} minimization [44], [45], expectation-maximization sparse Bayesian learning (EM-SBL) [13], and simultaneous orthogonal matching pursuit (SOMP) [46] algorithms are applied to recover the transmitted messages of MTDs using the received signal remaining after SIC of the eMBB devices.

• Finally, we provide a numerical performance analysis for the coexistence of the eMBB and MTC traffic. Our findings reveal that harmonious coexistence is viable when the operating point of the heterogeneous network is appropriately adjusted by tuning the average signal-to-noise ratio (SNR) and pilot length parameters.

C. Organization and Notation

The remainder of this paper is organised as follows. In Section II, we describe the system model. In Section III, we present the coherent data processing of the eMBB data, while in Section IV, we introduce the problem of non-coherent detection of MTDs. Section V deals with SSR algorithms for JADD. Section VI-A presents numerical results, and lastly, in Section VII, we draw the conclusions and recommend possible research directions.

Notation: Boldface lowercase and boldface uppercase letters denote column vectors and matrices, respectively. Moreover, a_i and a_{i,j} are the i-th column and the element in the i-row, j-th column of matrix A, respectively, while a_{i} is the i-th element of vector a. The superscripts (·)^T and (·)^H denote the conjugate transpose, and conjugate transpose operations, respectively. We denote the circularly symmetric complex Gaussian distribution with mean μ and covariance Σ by $\mathcal{CN}(\mu, \Sigma)$ while $\mathbb{E}\{\cdot\}$ is the expectation operator. If $D_1, \ldots, D_N$ are square matrices, then $D = \text{diag}(D_1, D_2, \ldots, D_N)$ creates a matrix whose block diagonal matrices are $D_1, D_2, \ldots, D_N$, while $\text{diag}(a_1, a_2, \ldots, a_n)$ creates a diagonal matrix whose main diagonal terms are $a_1, a_2, \ldots, a_n$. For both matrices and vectors, the hat notation indicates an estimate, e.g., $\hat{x}$ is the estimate of $x$; $\mathbb{C}$ and $\mathbb{R}$ refer to complex and real domains, respectively. Finally, $\|\|_F$ and $\|\|_p$ denote the Frobenius and $\ell_p$ norms, respectively and $(\cdot)^\text{c}$ is the binomial coefficient. Table I summarizes the main acronyms and symbols used in this paper.

II. SYSTEM MODEL

We consider a heterogeneous network depicted by Fig. 1(a), where a BS with an $M$-element array serves a set $N = \{1, \ldots, N\}$ of single-antenna MTDs and a set $E = \{1, \ldots, E\}$ of eMBB devices. The uplink transmission powers are $p_{e,n}^{UL}, e \in \mathcal{E}$, for the $e$-th eMBB device and $p_{n}^{UL}, n \in N$, for the $n$-th MTD. We assume that all $E$ eMBB devices are active in a coherence interval of $T$ symbols, while only $K$ out of the $N$ MTDs are active. The justification for this assumption is that eMBB devices are generally active for longer periods of time and usually apply scheduled access as opposed to MTDs, which only transmit short data messages with sporadic activation [47]. The set of active MTDs, denoted by $K \subseteq N$, is unknown to the BS. Moreover, the MTDs are assumed to activate with probability $\epsilon$ in each coherence interval, hence, on average $\epsilon N$ MTDs are active in each coherence interval. The channel between the $e$-th eMBB device and the BS is modelled as $h_e \sim \mathcal{CN}(0, \beta_e I) \in \mathbb{C}^{M \times 1}$ and between the $n$-th MTD and the BS as $g_n \sim \mathcal{CN}(0, \gamma_n I) \in \mathbb{C}^{M \times 1}$, where $\{\beta_e\}$ and $\{\gamma_n\}$ are the large scale fading coefficients. All devices are assumed to be stationary and, therefore, the BS knows $\{\beta_e\}$ and $\{\gamma_n\}$.

III. eMBB CHANNEL ESTIMATION AND DECODING

To enable coherent decoding of eMBB devices, the CSI of each eMBB device is acquired using a pilot sequence of $L$ symbols, while $T - L$ symbols are used for encoding the actual intended messages, i.e., payload transmission. This two-phase strategy is chosen because it is efficient to perform CSI estimation followed by payload transmission in eMBB services [8]. The signal received at the BS is a combination of the signals from the $E$ eMBB devices and the active MTDs, with a working assumption that $E < L$. In the symbol slot
\[ k \in \{1, 2, \cdots, T\}, \] the BS receives a signal \( \vec{y}[k] \in \mathbb{C}^{M \times 1} \) of the form
\[ \vec{y}[k] = \sum_{e=1}^{E} \sqrt{\rho_{e}^{UL}} s_{e}[k] \mathbf{h}_{e} + \sum_{n=1}^{N} \alpha_{n} s_{n}[k] \mathbf{g}_{n} + \mathbf{n}[k], \]
(1)

where \( \mathbf{g}_{n} = \sqrt{\frac{UL}{M}} \mathbf{g}_{n}, \alpha_{n} \in \{0, 1\} \) is the activity indicator for the \( n \)-th MTD, \( \mathbf{n}[k] \sim \mathcal{C}\mathcal{N}(\mathbf{0}, \sigma^{2} \mathbf{I}) \in \mathbb{C}^{M \times 1} \) is the additive white Gaussian noise (AWGN) at the receiver antennas, \( s_{n}[k] \) is the symbol transmitted by the \( n \)-th MTD in the \( k \)-th slot, with \( \mathbb{E}\{s_{n}[k]\}^{2} = \frac{1}{M} \), and \( s_{e}[k] \) is the symbol transmitted by the \( e \)-th eMBB device in the \( k \)-th slot, with \( \mathbb{E}\{s_{e}[k]\}^{2} = \frac{1}{M} \). The transmitted symbols by the \( e \)-th eMBB device are split into two parts as
\[ s_{e}[k] = \begin{cases} \psi_{e}[k], & k \in \{1, 2, \cdots, L\} \\ \phi_{e}[k], & k \in \{L+1, L+2, \cdots, T\} \end{cases}, \quad \forall e \in \mathcal{E}, \]
(2)

where \( \psi_{e} \in \mathbb{C}^{L \times 1} \) and \( \phi_{e} \in \mathbb{C}^{(T-L) \times 1} \) are vectors containing the pilot and payload data for the \( e \)-th eMBB device, respectively (refer to Fig. 1(b)). At this stage, it is important to mention that for symbol slots \( k \in \{1, 2, \cdots, L\} \), \( \{\psi_{e}\} \) are mutually orthogonal, i.e., \( \psi_{i}^{H} \psi_{j} = 0, i, j \in \mathcal{E}, \) with \( i \neq j \), and also designed to be orthogonal to \( \{s_{n}[1], s_{n}[2], \cdots, s_{n}[L]\}^{T}, \forall n \in \mathcal{N} \). The details of this joint pilot and signature sequence design are provided in Section IV-B. The orthogonality in slots \( k \in \{1, 2, \cdots, L\} \) is the key feature utilized to accurately acquire CSI estimates of the eMBB devices, as will be discussed next.

### A. Channel Estimation

At the symbol slots \( k \in \{1, 2, \cdots, L\} \), the \( L \) received symbols at the BS are
\[ \mathbf{Y}_{p} = [\vec{y}[1], \vec{y}[2], \cdots, \vec{y}[L]]^{T}, \]
(3)

which are subsequently used in the correlation process to compute the received pilot signal from each eMBB device, \( \mathbf{y}_{e} \in \mathbb{C}^{M \times 1} \), as
\[ \mathbf{y}_{e} = \mathbf{Y}_{p}^{H} \psi_{e}^{*} = \mathbf{h}_{e} \psi_{e}^{*} + \mathbf{N}_{p} \psi_{e}^{*}, \quad \forall e \in \mathcal{E}, \]
(4)

where
\[ \mathbf{N}_{p} = [\mathbf{n}[1], \mathbf{n}[2], \cdots, \mathbf{n}[L]] \in \mathbb{C}^{M \times L}. \]

Note that due to the mutual orthogonality of \( \{\psi_{e}\} \) and orthogonality to the first \( L \) symbols transmitted by the MTDs, the processed signal \( \mathbf{y}_{e} \) is free from interference of other eMBB devices and the MTDs. This in turn enables accurate estimation of the CSI of the \( e \)-th eMBB device, thus promoting coexistence of eMBB and MTDs.

To obtain a CSI estimate of the \( e \)-th eMBB device, the BS uses the MMSE estimator [48]
\[ \hat{\mathbf{h}}_{e} = \sqrt{\frac{UL}{\rho_{e}^{UL}}} \mathbf{p}_{e} \mathbf{y}_{e}, \]
(5)

where \( \mathbf{p}_{e} = (\sigma^{2} + \beta_{e})^{-1} \mathbf{I} \in \mathbb{C}^{M \times M} \) is the covariance matrix of \( \mathbf{y}_{e} \). It then follows that the MMSE estimate, \( \hat{\mathbf{h}}_{e} \), and the estimation error \( \mathbf{h}_{e} = \hat{\mathbf{h}}_{e} - \mathbf{h}_{e} \) are distributed as [48]
\[ \hat{\mathbf{h}}_{e} \sim \mathcal{C}\mathcal{N}(\mathbf{0}, \mathbf{p}_{e}) \]

respectively, where \( \mathcal{E}_{e} \in \mathbb{C}^{M \times M} \) is the covariance matrix of the estimation error, defined as
\[ \Sigma_{e} = \mathbf{I} - \mathbf{L}^{UL}_{e} \mathbf{p}_{e}^{2} \mathbf{I}. \]
(6)

### B. Data Decoding

We assume that the BS uses the MMSE combiner [49] to decode the signals from the eMBB devices. In general, the BS’ ability to accurately decode the eMBB signals is subject to the accuracy of the channel estimate \( \hat{\mathbf{h}}_{e} \). This impact can be captured by the signal-to-interference plus noise ratio (SINR), which for each eMBB device is given by (7), shown at the bottom of the next page, where \( \mathbf{w}_{e} = (\sigma^{2} + \beta_{e})^{-1} \sum_{j \in \mathcal{E} \neq e} \mathbf{h}_{j} \mathbf{h}_{j}^{H} \mathbf{h}_{e} \) is the receive combiner. The value of \( \mathbf{w}_{e} \) depends on \( \hat{\mathbf{h}}_{e} \) and therefore introduces the estimation error into the SINR.

The expression (7) is defined differently from works such as [8] because we assume that the symbols can be correlated, e.g., MTDs can have similar messages, as will be seen in Section IV-B. Nevertheless, \( \Gamma_{e} \), can be interpreted as the measure of how much the signal from the \( e \)-th eMBB device is buried in the network. As a result, the probability of decoding errors tends to be lower for devices with relatively high values of \( \Gamma_{e} \) as compared to those with lower values. To facilitate non-coherent decoding of the MTDs, the BS removes signal contribution of devices that were correctly decoded from \( \vec{y} \) in (1) using SIC. As a result, the coexistence of the eMBB devices and MTDs, is affected by how accurate the SIC is performed.
IV. Joint Activity Detection and Decoding of MTDs

A. Non-Coherent Decoding of MTDs

Non-coherent signal recovery promises to reduce the access latency caused by the need to acquire explicit CSI before data decoding [8], [50]. This is specifically appealing for short packet communications such as in MTC. In order to convey data non-coherently from MTDs, each of the MTDs is pre-allocated \( Q \) different messages. Under this scenario, each active MTD can strictly transmit one selected message in a given coherence interval. From CS-MUD perspective, recovery of these messages can be achieved by joint activity and data decoding (JADD).

It is important to highlight that due to the heterogeneity of the network, the BS recovers the messages from the MTDs after \( T \) symbols have collectively been used for CSI estimation, decoding, and SIC of correctly decoded eMBB signals. Ideally, after processing the eMBB data, the remaining signals. Ideally, after processing the eMBB data, the remaining CSI estimation, decoding, and SIC of correctly decoded eMBB data as

\[
\mathbf{Y} = \sum_{n=1}^{N} \sum_{q=1}^{Q} \alpha_n^q \mathbf{s}_n^q \mathbf{g}_n^T + \mathbf{W},
\]

where \( \mathbf{W} \in \mathbb{C}^{T \times M} \) comprises both the receiver noise and the resultant residual interference from imperfect SIC (due to errors in the CSI estimation of the eMBB devices). The \( m \)-th column of \( \mathbf{W} \) is denoted by \( w_m = [w_{m1}, w_{m2}, \ldots, w_{mL}]^T \), where \( w_m \sim \mathcal{CN}(0, \sigma^2 \mathbf{I} + \sum_{e=1}^{E} \mathbf{Z}_e) \in \mathbb{C}^{L \times 1} \) is the combination of the AWGN and the error vector during eMBB training and \( \mathbf{w}_d \in \mathbb{C}^{(T-L) \times 1} \) models the combination of the AWGN and the possible error vector due to eMBB decoding followed by imperfect SIC. Note that the structure of \( \mathbf{w}_d \) depends on the accuracy of SIC, as discussed in Section III-B. It is therefore important to note that even though there will be varying degrees of accuracy of SIC, there are two special cases: i) when SIC is perfect, \( \mathbf{w}_d \) reduces to AWGN and ii) when SIC is not performed, \( \mathbf{w}_d \) reduces to the deterministic composite signal of eMBB devices, i.e., \( \sum_{e=1}^{E} \sqrt{\rho_c} \mathbf{e}_e \).

From the preceding discussion, the BS processes \( \mathbf{Y} \) with the intention to recover \( \alpha \). To reveal the sparsity pattern in \( \alpha \), we rewrite the signal (10) in its matrix-equivalent form as

\[
\mathbf{Y} = \sum_{n=1}^{N} \left[ \begin{array}{c} \mathbf{s}_1^1, \mathbf{s}_2^1, \ldots, \mathbf{s}_Q^1 \\ \vdots \\ \mathbf{s}_1^Q, \mathbf{s}_2^Q, \ldots, \mathbf{s}_Q^Q \end{array} \right] \begin{bmatrix} \alpha_1^1 & \cdots & \alpha_Q^1 \\ \vdots & \ddots & \vdots \\ \alpha_1^Q & \cdots & \alpha_Q^Q \end{bmatrix} \begin{bmatrix} \mathbf{g}_1^T \\ \vdots \\ \mathbf{g}_Q^T \end{bmatrix} + \mathbf{W},
\]

\[
= \sum_{n=1}^{N} \mathbf{S}_n \mathbf{D}_n \mathbf{G}_n + \mathbf{W} = \mathbf{SDG} + \mathbf{W},
\]

where \( \mathbf{S} = [\mathbf{S}_1, \mathbf{S}_2, \ldots, \mathbf{S}_N] \in \mathbb{C}^{T \times NQ} \) is a collection of all the message sequences allocated to the MTDs, \( \mathbf{D} = \text{diag}(\mathbf{D}_1, \mathbf{D}_2, \ldots, \mathbf{D}_N) \in \mathbb{R}^{NQ \times NQ} \) is the (sequence) activity indicator matrix with \( \mathbf{D}_n = \text{diag}(\alpha_1^1, \alpha_2^1, \ldots, \alpha_Q^1) \in \{0, 1\}^{Q \times Q} \), and \( \mathbf{G} = [\mathbf{G}_1^T, \mathbf{G}_2^T, \ldots, \mathbf{G}_N^T] \in \mathbb{C}^{NQ \times M} \). In this context, we are trying to solve for \( \mathbf{S}_n \), i.e.,

\[
\mathbf{S}_n = \left( \sum_{k=L+1}^{T} \left( \sum_{i \in \mathcal{K}} \sqrt{\rho_c} |\mathbf{g}_i^h s_i[k]|^2 + \sum_{j \in \mathcal{E} \neq c} \sqrt{\rho_c} |\mathbf{g}_j^h h_{ij} s_j[k]|^2 + \sqrt{\rho_c} |\mathbf{g}_c^h h_{ic} s_c[k]|^2 + |\mathbf{g}_c^h n[k]|^2 \right) \right)^{-1} \sum_{k=L+1}^{T} \sqrt{\rho_c} |\mathbf{g}_c^h h_{ic} s_c[k]|^2
\]

(7)
matrix comprising repeated effective channels of the \( n \)-th MTD. The received signal is

\[
Y = SX + W,
\]

where \( X = DG \in \mathbb{C}^{NQ \times M} \) is a row-sparse matrix. Explicitly, the sparse rows of \( X \) can be represented by

\[
X = \begin{bmatrix}
X_1 & X_2 & \cdots & X_N
\end{bmatrix} = \begin{bmatrix}
\alpha_1^1 g_{11}, g_{12}, \ldots, g_{1M} \\
\alpha_1^2 g_{11}, g_{12}, \ldots, g_{1M} \\
\vdots & \ddots & \ddots & \vdots \\
\alpha_q^1 g_{n1}, g_{n2}, \ldots, g_{nM} \\
\vdots & \ddots & \ddots & \vdots \\
\alpha_q^N g_{n1}, g_{n2}, \ldots, g_{nM}
\end{bmatrix},
\]

where \( X_n = D_nG_n \in \mathbb{C}^{Q \times M} \) is the \( n \)-th sub-matrix of \( X \) and \( x_{nq}^q = \alpha_n^q g_{nq}^q \) is the effective channel of the \( n \)-th MTD when transmitting its \( q \)-th sequence, thus, corresponding to row number \((n-1)Q + q \) of \( X \). Recall that the row sparsity of \( X \) has a special structure: each \( X_n \) can have at most one non-zero row. Note that, with the structure in (13), the non-zero entries of \( X \) occur with probability \( \xi = \frac{1}{Q} \), even though the activation probability of MTDs is \( \epsilon \). Alternatively, by using this row sparsity, each sequence can be interpreted as a fictitious device.

From (12), \( Y \in \mathbb{C}^{T \times M} \) is a noisy compressed measurement of \( X \). It then follows that the JADD task is to recover \( X \) from \( Y \) with the knowledge of \( S \) by using some sparsity-promoting operation, \( f(\cdot) \), resulting in an estimate of \( X \) as \( \hat{X} = f(Y; S) \). From this viewpoint, the efficacy of \( f(\cdot) \) is inherently improved by optimizing \( S \). To this end, we propose an algorithm for generating message sequences \( S \) for MTDs in Section IV-B, while the formal JADD problem and its algorithmic solutions are presented in Section V.

### B. Joint Generation of eMBB Pilots and MTD Sequences

Like motivated in Section III-A, successful coexistence of eMBB and MTC traffic requires that each pilot sequence \( \psi_e \) be orthogonal to the data of the MTDs in the first \( L \) symbol slots. Consistent with this requirement, we propose a joint generation of \( S \) and \( \{ \psi_e \} \).

First, we handle the assignment of the pilot sequences to the \( E \) eMBB devices. We generate \( L \) orthogonal sequences \( \{c_1, c_2, \ldots, c_L\} \in \mathbb{C}^{L \times L} \) using a complex-valued Hadamard matrix,\(^2\) whose columns and rows are mutually orthogonal, i.e., \( c_i^j c_j = 0, \forall i \neq j \). Then, without loss of generality, we let \( \psi_1 = c_1, \psi_2 = c_2, \ldots, \psi_E = c_E \).

Once \( \{ \psi_e \} \) are assigned to the \( E \) eMBB devices, then there are \( L - E \) orthogonal sequences remaining to be allocated to the MTDs for the first \( L \) symbol slots. To facilitate the presentation, we decompose each message sequence of the \( n \)-th MTD as \( s_n^q = (v_n)^{T}, (u_n^q)^{T} \), \( q = 1, \ldots, Q \), where \( v_n \in \mathbb{C}^{L \times 1} \) and \( u_n^q \in \mathbb{C}^{(T-L) \times 1} \) are the message (sub)sequences for slots \( \{1, \ldots, L\} \) and \( \{L + 1, \ldots, T\} \), respectively. Note that the message sequences of the \( n \)-th MTD, \( s_n^q, q = 1, \ldots, Q \), share the same “header” \( v_n \), while their second parts \( u_n^q \) are unique. Next, we address the design of each \( v_n, n \in N \).

Given that \( L - E \ll N \), it is not feasible to allocate orthogonal sequences to each MTD to create \( v_n, n \in N \). In addition, the requirement that \( \{v_n\} \) has to be orthogonal to \( \{\psi_e\} \) makes it necessary to reuse the remaining \( L - E \) orthogonal pilot sequences for multiple MTDs. However, this poses a risk of possible high correlations between the pilot sequences \( \{v_n\} \). Such highly correlated pilot sequences can lead to ambiguities during identification of the MTDs by means of mutual interference. Evidently, these ambiguities result in degradation in the performance of the receiver. To avert this challenge, we devise a pilot design strategy that can mitigate the mutual interference between the MTDs by maintaining high incoherence between each \( v_n \). We do this as follows. Let \( B = \{c_{E+1}, \ldots, c_L\} \) be the set of the \( L - E \) remaining orthogonal sequences after assigning \( \{\psi_e\} \) to the eMBB devices. The sequence \( v_n \) of the \( n \)-th MTD is formed by randomly selecting a subset of orthogonal sequences in \( B \) which are then linearly combined using random weights.\(^3\) More precisely, let \( \pi_n = \{\pi_n(1), \ldots, \pi_n(z)\} \) be a collection of indices associated with the random sequence selection, where \( \pi_n(l) \in \{E + 1, \ldots, L\} \). Here, \( z < L \) is a parameter that adjusts how many sequences each MTD can combine. Note that as \( z \) increases, more orthogonal columns are combined and as such, more highly correlated pilot sequences are generated. We address this by minimizing the probability that two devices have the same \( v_n \), hence ensuring that each MTD can be identified without ambiguity. To achieve this, we fix a reasonable maximum collision probability \( \chi \) and find the minimum value of \( z \) that attains this probability. Hence, we solve an integer problem

\[
\begin{align*}
\text{minimize} \quad & z \\
\text{subject to} \quad & \frac{1}{z} \leq \chi,
\end{align*}
\]

where \( \chi \) is the target collision probability.\(^4\)

The problem (14) does not have a closed-form solution. We therefore exhaustively search over possible values of \( z \), and pick the minimum value of \( z \) that satisfy the collision probability constraint. Note that the search is done simply over the positive integers and is thus of low complexity. Fig. 2 illustrates the collision probability as a function of \( z \), for \( E = 4 \). The values of \( z \) that solve (14) for the targeted collision

\(^3\)Power normalization of the entire message sequence \( s_n^q \) is done later.

\(^4\)It is important to note that the value of \( \chi \) is high for small \( L \), and thus impractical to set similar values of \( \chi \) for all values of \( L \). For example, for \( L = 8 \), the lowest achievable collision probability is \( \chi = 0.1 \). In this case, \( z \) is set to any value below \( L - E \). For \( L \geq 32 \), a common \( \chi \) can be used.
To conclude, by constructing a collection of sequences, another. Our proposed sequence optimization is presented in Algorithm 1. To further enhance the JADD of the MTDs, sub-sequences are generated from the modulation alphabet of order $\kappa$. In Line 2, the cross-correlation matrix $\Theta$ is computed, which captures the amount of correlation between any pairs of candidate sequences in $\hat{U}_n$. Subsequently, the iterative procedure in Lines 4–6 utilizes $\Theta$ to assign unique sequences (i.e., rows of $\hat{U}_n$) that yield the minimal cross-correlation. Line 4 gives the $i^*$-th and $j$-th rows that are least correlated. In Line 5, the $q$-th sub-sequence of MTD $n$ is assigned based on the index $i^*$, i.e., $u^q_n = \hat{U}_{n,i^*}$. Line 6 prevents reuse of the $i^*$-th sequence of $\hat{U}_n$. The complexity of the proposed algorithm is $O \left( \left( \frac{(e^{T-L})^2}{2} \right)^2 + (T-L)e^{T-L} \right)$. Evidently, this is a high complexity algorithm. However, since MTDs generally have constant messages, the algorithm can be run once and only updated when a new device is added to the network.

V. SPARSE SIGNAL RECOVERY ALGORITHMS FOR JADD

To perform JADD after employing the SIC of the decoded eMBB signals, it should be noted that the effective channel matrix $X$ in (13) is strictly (row-)sparse and can be recovered using SSR techniques for a multiple measurement vector (MMV) problem. In our problem, we note the following special structures of $X$: i) the rows of $X$ are sparse as shown in (13), and ii) each $D_n$ has at most one non-zero element in its diagonal, hence imposing a restriction that at most one row of $X_n$ is non-zero. Taking this structure into consideration, the canonical form for the JADD problem can be formulated as

\[
\text{minimize}_{X} \frac{1}{2} \| Y - SX \|_F^2 + \mu \| X \|_{2,0}
\]

subject to $\text{Rank}(D_n) \leq 1, \forall n \in \mathcal{N}$,

where $X_{2,0} = \| x_{11} \|_2, \ldots, \| x_{NQ} \|_2$ enforces the sparsity along the rows of $X$ and $\mu > 0$ is a regularization parameter. However, we note that the problem (16) is non-convex and thus hard to solve. The non-convexity arises due to the fact that i) the objective function (16a) is non-convex and ii) the rank constraint (16b) is non-convex.

To provide solution to problem (16), the JADD problem is solved in two steps. First, we consider tractable solutions to the problem (16a) by neglecting constraint (16b). Thereafter, use a two-step simplification which incorporates the rank constraint by hard-thresholding.

Algorithm 1 Generation of Messages $u^q_n$, $q = 1, \ldots, Q$ for Each MTD $n$

1. Input: A matrix of all possible messages $\hat{U}_n = [\hat{u}^1_n, \hat{u}^2_n, \ldots, \hat{u}^T_n] \in \mathbb{C}^{e^{T-L} \times (T-L)}$
2. Compute $\Theta = |\hat{U}_n^\dagger \hat{U}_n|$
3. For $q = 1, \ldots, Q$:
   4. \{i^*, j\} = $\arg \min_{i,j \in \{1, 2, \ldots, e^{T-L}\}, \ i \neq j} \Theta_{i,j}$
5. $u^q_n = \hat{U}_{n,i^*}$
6. Set $\Theta_{i^*, j} = \infty$ for all $j = \{1, 2, \ldots, e^{T-L}\}$
7. End for

$5$ The details of SBL will be presented later in Section V.

$6$ In this work, we do not pursue for a tractable (convex) penalty function to incorporate the rank constraint into the optimization process. We instead use a two-step simplification which incorporates the rank constraint by hard-thresholding.

sequences in its rows, generated from the modulation alphabet of order $\kappa$. In Line 2, the cross-correlation matrix $\Theta$ is computed, which captures the amount of correlation between any pairs of candidate sequences in $\hat{U}_n$. Subsequently, the iterative procedure in Lines 4–6 utilizes $\Theta$ to assign unique sequences (i.e., rows of $\hat{U}_n$) that yield the minimal cross-correlation. Line 4 gives the $i^*$-th and $j$-th rows that are least correlated. In Line 5, the $q$-th sub-sequence of MTD $n$ is assigned based on the index $i^*$, i.e., $u^q_n = \hat{U}_{n,i^*}$. Line 6 prevents reuse of the $i^*$-th sequence of $\hat{U}_n$. The complexity of the proposed algorithm is $O \left( \left( \frac{(e^{T-L})^2}{2} \right)^2 + (T-L)e^{T-L} \right)$. Evidently, this is a high complexity algorithm. However, since MTDs generally have constant messages, the algorithm can be run once and only updated when a new device is added to the network.

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where $X_{2,0} = \| x_{11} \|_2, \ldots, \| x_{NQ} \|_2$ enforces the sparsity along the rows of $X$ and $\mu > 0$ is a regularization parameter. However, we note that the problem (16) is non-convex and thus hard to solve. The non-convexity arises due to the fact that i) the objective function (16a) is non-convex and ii) the rank constraint (16b) is non-convex.

To provide solution to problem (16), the JADD problem is solved in two steps. First, we consider tractable solutions to the problem (16a) by neglecting constraint (16b). Thereafter, use a two-step simplification which incorporates the rank constraint by hard-thresholding.

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2. Compute $\Theta = |\hat{U}_n^\dagger \hat{U}_n|$
3. For $q = 1, \ldots, Q$:
   4. \{i^*, j\} = $\arg \min_{i,j \in \{1, 2, \ldots, e^{T-L}\}, \ i \neq j} \Theta_{i,j}$
5. $u^q_n = \hat{U}_{n,i^*}$
6. Set $\Theta_{i^*, j} = \infty$ for all $j = \{1, 2, \ldots, e^{T-L}\}$
7. End for

$5$ The details of SBL will be presented later in Section V.

$6$ In this work, we do not pursue for a tractable (convex) penalty function to incorporate the rank constraint into the optimization process. We instead use a two-step simplification which incorporates the rank constraint by hard-thresholding.
an estimate of $\ell_2$-norms of each row of $\hat{X}$ is computed at the BS as

$$\hat{x} = [\|\hat{x}_{n1}\|_2, \|\hat{x}_{n2}\|_2, \ldots, \|\hat{x}_{nQ}\|_2]^{T}. \quad (17)$$

Let $x_n = [\|\hat{x}_{n1}\|_2, \ldots, \|\hat{x}_{nQ}\|_2]^{T} \in \mathbb{R}^{Q \times 1}$ be the norms of all the $Q$ rows corresponding to the $n$-th MTD. The constraint (16b) is incorporated by thresholding $\hat{x}$ the maximum entry of $x_n$ using $\zeta$. Hence, the estimated sequence transmission indicator for each $q$-th sequence is

$$\hat{\alpha}_n^q = \begin{cases} 1, & \text{if } \max\{x_{n}\} \geq \zeta \\ 0, & \text{otherwise} \end{cases}. \quad (18)$$

Given a potentially massive number of MTDs and that each can be allocated more than one message sequence, the problem of solving for $X$ is high-dimensional. As a remedy, we exploit computationally efficient iterative SSR procedures\cite{8},\cite{21},\cite{54}, the ADMM based $\ell_2,1$-minimization algorithm\cite{44},\cite{55}, EM-SBL\cite{56} and SOMP\cite{57} are discussed next. Moreover, since a typical 5GB cellular network is composed of a massive number of MTDs coexisting with eMBB devices, then the computational complexity of the algorithms running at the BS is of critical importance as it influences power consumption and contributes to the carbon footprint. Table II presents a summary of the complexity of each SSR algorithm.

### A. Solution via Approximate Message Passing (AMP)

The AMP utilised in this work is based on the Bayesian denoiser\cite{8},\cite{21},\cite{54}. From statistical point of view, AMP enforces sparsity by treating each row of $X$ as a vector independently generated from the distribution

$$p(x_{nq}) = (1 - \xi)\delta_0(x_{nq}) + \xi C_N(x_{nq}; 0, \gamma_n I), \quad (19)$$

where $\delta_0(x_{nq})$ is the Dirac delta function defined as

$$\delta_0(x_{nq}) = \begin{cases} \infty, & \text{if } x_{nq} = 0 \\ 0, & \text{otherwise} \end{cases}. \quad (20)$$

and satisfying $\int_{x_{nq}} \delta_0(x_{nq})dx_{nq} = 1$.

From (19), $x_{nq} = 0$ with probability $1 - \xi$ and $x_{nq} \sim C_N(0, \gamma_n I)$ with probability $\xi$. Based on this prior distribution, the AMP procedure utilises $Y$ to find the estimate $\hat{X}$ that minimizes the mean squared error (MSE)

$$\text{MSE} = \mathbb{E}_{X,Y} \| \hat{X}(Y) - X \|_2^2. \quad (21)$$

### Algorithm 2 AMP Decoding

**Input**: $Y$, $\Delta$, $\eta$

1. Initialization: $\hat{X}^0 = 0$, $R^0 = Y$, $t = 0$

2. repeat

3. $\hat{x}_{nq}^{t+1} = \eta((R^t)^{H}x_{nq}^t) \forall n, \forall q$

4. $R^{t+1} = Y - SX^{t+1} + \frac{\gamma}{NQ} \langle (\hat{R})^Hx_{nq}^t + \hat{x}_{nq}^t \rangle$

5. $\hat{\Sigma}^{t+1} = \frac{\sigma^2 I}{\mathbb{P}_M} + \frac{\gamma}{NQ} \mathbb{E}(ee^H)$

6. $t = t + 1$

7. until $\|R^{t+1} - R^t\|_F < \Delta$

**Output**: $\hat{X} = X$

Algorithm 2 presents details of the minimization steps of (21). Line 1 is the initialization step, where the estimate $\hat{X}^t \in \mathbb{C}^{NQ \times M}$ and residual $R^t \in \mathbb{C}^{T \times M}$ at the iteration index $t$ are set to zero. The iterative procedure is repeated between Lines 2 and 6 until convergence. Line 3 computes the current estimate $\hat{x}_{nq}^{t+1}$ using the MMSE denoising function defined as [8], [21]

$$\eta(x_{nq}, \Sigma) = \frac{\gamma_n (\gamma_n I + \Sigma)^{-1}x_{nq}}{1 + \frac{\gamma_n}{\xi} (\delta(x_{nq})/\text{det}(I + \gamma_n \Sigma)^{-1})}, \quad (22)$$

where $\delta(x_{nq}) = \exp(-x_{nq}^H\Sigma^{-1}x_{nq}) + x_{nq}^H(\gamma_n I + \Sigma)^{-1}x_{nq}$. Line 4 computes the residual and $\eta$ is the element-wise first order derivative of $\eta$, hence it is a diagonal matrix for each $x_{nq}$. The $\langle \rangle$ operator computes the average over all the $NQ$ matrices. It can be observed that (22) depends on $\Sigma$, which is referred to as the state evolution [21]. This is a metric that measures the average MSE in Line 5, where $e = \eta(x_{nq} + (\Sigma)^{1/2} \nu) - x_{nq}$, and $\nu \sim C_N(0, I) \in \mathbb{C}^{M \times 1}$ is a random error independent of $x_{nq}$.

### B. Solution via ADMM Based $\ell_2,1$-Minimization

The design of the AMP denoising function described in Section V-A depends heavily on the fact that the large scale fading coefficients $\gamma_n$, $n = 1, \ldots, N$, and activation probability $\epsilon$ are known at the BS. However, if such information is not available at the BS, for instance, when a device is not active for a long time, mixed-norm minimization approaches [58] constitute a viable solution as they are insensitive to the prior distribution. In practice, the most commonly used mixed-norm
minimization approach is the $\ell_{2,1}$-norm minimization, given as
\[
\min_{\mathbf{X}} \frac{1}{2} \| \mathbf{Y} - \mathbf{S}\mathbf{X} \|^2_F + \mu \| \mathbf{X} \|_{2,1},
\]
(23)
where $\mathbf{X}_{2,1} = \| \mathbf{x}_{11} \|_2, \cdots, \| \mathbf{x}_{NQ} \|_2 \|_1$. Note that the problem (23) is convex and can be solved optimally using standard convex optimization method and solvers such as cvx [45]. However, since the expected number of devices is high in MTC, this approach is rendered highly inefficient.

Motivated by the need for a computationally efficient solution to (23), we next present an iterative solution via an ADMM framework, where the update equations are in closed-form. First, we introduce an auxiliary variable $\mathbf{Z} \in \mathbb{C}^{NQ \times M}$ and rewrite (23) as
\[
\min_{\mathbf{X}, \mathbf{Z}} \frac{1}{2} \| \mathbf{Y} - \mathbf{S}\mathbf{Z} \|^2_F + \mu \| \mathbf{X} \|_{2,1}
\]
subject to $\mathbf{Z} = \mathbf{X}$.

(24b)

Subsequently, the augmented Lagrangian associated with problem (24) is given as
\[
\mathcal{L}(\mathbf{X}, \mathbf{Z}, \Lambda) = \frac{1}{2} \| \mathbf{Y} - \mathbf{S}\mathbf{Z} \|^2_F + \mu \| \mathbf{X} \|_{2,1} + \frac{\rho}{2} \| \mathbf{S} - \mathbf{Z} + \frac{\Lambda}{\rho} \|^2_F,
\]
(25)
where $\Lambda = [\lambda_{1,1}, \cdots, \lambda_{1,Q}, \cdots, \lambda_{N,1}, \cdots, \lambda_{N,Q}]^T \in \mathbb{C}^{NQ \times M}$ is the matrix of ADMM dual variables and $\rho$ is a positive parameter that controls the convergence speed of ADMM [44]. The solution to problem (24) via ADMM is achieved by sequentially updating ($\mathbf{X}, \mathbf{Z}, \Lambda$) as follows
\[
\mathbf{Z}^{t+1} := \min_{\mathbf{Z}} \frac{1}{2} \| \mathbf{Y} - \mathbf{S}\mathbf{Z} \|^2_F + \frac{\rho}{2} \| \mathbf{X}^{t+1} - \mathbf{Z}^{t+1} + \frac{1}{\rho} \Lambda^{t+1} \|^2_F,
\]
(26)
\[
\mathbf{X}^{t+1} := \min_{\mathbf{X}} \mu \| \mathbf{X} \|_{2,1} + \frac{\rho}{2} \| \mathbf{X}^{t+1} - \mathbf{Z}^{t+1} + \frac{1}{\rho} \Lambda^{t+1} \|^2_F,
\]
(27)
\[
\Lambda^{t+1} := \Lambda^{t} + \rho (\mathbf{X}^{t+1} - \mathbf{Z}^{t+1}).
\]
(28)

The ADMM solution is detailed in Algorithm 3. Step 3 is the update for $\mathbf{Z}$. It is obtained by setting the derivative of the convex objective function (26) to zero and solving for $\mathbf{Z}$. The $\mathbf{X}$-update in Line 5 is computed using the soft-thresholding operator [44], by decoupling (27) into $NQ$ convex subproblems (for $n = 1, \cdots, N$ and $q = 1, \cdots, Q$) as
\[
\mathbf{x}_{nq}^{t+1} := \min_{\mathbf{x}_{nq}} \{ \frac{1}{2} \| \mathbf{x}_{nq} \|_2^2 + \frac{\rho}{2} \| \mathbf{x}_{nq} - \mathbf{z}_{nq}^{t+1} + \frac{1}{\rho} \lambda_{nq} \|_F^2 \},
\]
(29)

C. Solution via Expectation-Maximization Sparse Bayesian Learning

Sparse Bayesian learning (SBL), an important family of Bayesian SSR algorithms, recovers a sparse vector through a hierarchical signal prior model. The key is to introduce real-valued hyperparameters, $\alpha = \{\alpha_{nq}\}_{n \in N, q = 1, \cdots, Q}$, which represent the (co)variance of each Gaussian channel $\{g_n\}$. The main task in SBL is to estimate the sparse vector $\alpha$, which consequently reveals the underlying sequence transmission indicator $\alpha$. In SBL, for a given $\alpha$, the signal estimate is given as the MMSE estimate [13], $\mathbf{X} = \mathbb{E}[\mathbf{X}\mid \mathbf{Y}, \alpha]$, which is linear due to Gaussianity (see Line 3 in Algorithm 4); here,

Algorithm 3 ADMM Decoding

Input: $\mathbf{Y}, \Delta$

1. Initialization: $\mathbf{X}^0 = \mathbf{0}, \mathbf{Z}^0 = \mathbf{0}, \Lambda^0 = t = 0$

2. repeat

3. $\mathbf{z}_{nq}^{t+1} = (\rho^{\mathbf{X}^{t+1}} + \mathbf{1} + \mathbf{Y}^T \mathbf{S}^T \mathbf{S} + \mathbf{R}_{NQ}^{-1})^{-1}

4. $\mathbf{c}_{nq} = (\mathbf{z}_{nq}^{t+1} - \mathbf{1} \lambda_{nq} \mathbf{v}_q, \forall n)

5. $\mathbf{z}_{nq}^{t+1} = \max(0, \mathbf{c}_{nq}) \mathbf{v}_q, \forall n)

6. $\Lambda^{t+1} = \Lambda^t + \rho(\mathbf{X}^{t+1} - \mathbf{Z}^{t+1})$

7. $t = t + 1$

until $\| \mathbf{Z}^{t+1} - \mathbf{Z}^t \|_F < \Delta$

Output: $\mathbf{X} = \mathbf{Z}^t$

Algorithm 4 EM-SBL Decoding

Input: $\mathbf{Y}, \Delta, \sigma^2$

1. Initialization: $\mathbf{X}^0 = \mathbf{0}, \bar{\alpha} = 1_{NQ \times 1}, t = 0$

2. repeat

3. $\mathbf{x}^t = \mathbf{Y}^t = (\Sigma + \mathbf{S}^T \mathbf{S})^{-1} \mathbf{Y}$

4. $\mathbf{F}^t = \left( \mathbf{Y}^t + \frac{1}{\sigma^2} \mathbf{S}^T \mathbf{S} \right)^{-1} \mathbf{Y}$

5. $\bar{\alpha} = \pi \| \mathbf{x}_{nq}^t \|^2_2 + \mathbf{F}_{ni}, i = 1, 2, \cdots, NQ, \forall n, \forall q$

6. $t = t + 1$

7. until $\| \mathbf{x}^{t+1} - \mathbf{x}^t \|^2_F < \Delta$

Output: $\mathbf{X} = \mathbf{X}^t$

\[
\bar{\alpha} = \arg\max_{\alpha} \log p(\bar{\alpha} \mid \mathbf{Y})
\]

$\bar{\alpha} = \arg\min_{\alpha} T \log |\Sigma| + \text{Tr} (\Sigma^{-1} \mathbf{Y} \mathbf{Y}^H) - p(\bar{\alpha}),$

(30)

where $\Sigma = \sigma^2 I + \mathbf{S}^H \mathbf{S}$ is the covariance matrix of the signal remaining after SIC of eMBB signals; $p(\bar{\alpha})$ is the sparsity-promoting prior distribution of the hyperparameter. In this work, non-informative $p(\bar{\alpha})$ is used, hence it has no impact in the minimization.

We solve (30) via expectation-maximization (EM) [13], hence the name EM-SBL. The iterative solution is presented in Algorithm 4. Line 3 updates the estimate of $\mathbf{X}$, whereas Line 5 updates the sparsity-promoting hyperparameter.

D. Solution via SOMP

The SOMP algorithm [46], [59] identifies the non-zeros entries of the sparse matrix $\mathbf{X}$ by iteratively selecting the columns of $\mathbf{S}$ that have the highest correlation with the residual $\mathbf{R}$ at each step. It is presented as Algorithm 5. Initially, the residual $\mathbf{R}$ is set to be equal to the version of $\mathbf{Y}$ that remains after SIC of the eMBB signals. Line 3 computes the correlation between $\mathbf{S}$ and the current residual, while Line 4 selects the column of $\mathbf{S}$ that has the highest correlation with $\mathbf{R}$. These columns are accumulated in $\mathbf{H}$ in Line 5. To avoid repetition,
in Line 7, the selected columns’ contributions are removed from Y, thus leaving a residual that is orthogonal to the previously selected columns.

Algorithm 5 SOMP Decoding

Input: \(Y, \Delta\)

1. Initialization: \(X^0 = 0, R^0 = Y, t = 0, H^{[0]} = \emptyset\)
2. repeat
3. \(G^t = S^H R^{t-1}\)
4. \(j^t = \arg \max_j \left\{ \left\| G^t_j \right\|_1 \right\} \)
5. \(H^t = H^{t-1} \cup j^t\)
6. \(X^t[\cdot] = S^H[\cdot] Y\)
7. \(R^t = Y - S X^t\)
8. \(t = t + 1\)
9. until \(\left\| X^t - X^{t-1} \right\|_F^2 < \Delta\)

Output: \(X = X^t\)

VI. NUMERICAL RESULTS AND DISCUSSIONS

In this section, we present numerical results to show the performance of our proposed framework in terms of the average outage probability, sequence detection accuracy, and channel estimation accuracy.

A. Simulation Setup

We consider a single-cell network of radius 250 m, where the BS serves \(N = 1000\) MTDs and \(E = 4\) eMBB devices, all randomly placed in the cell area. The path-loss for each device is computed as a function of the device’s distance \(d_i, i \in \{E \cup N\}\), from the BS. We adopt a power control mechanism which ensures that the average received power is the same for all the transmitted messages, irrespective of the device’s position. Since the large scale parameters are known at the BS, each MTD transmits with power

\[ p_{UL}^i = \frac{p_{\text{max}} \gamma_{\text{min}}}{\gamma_i}, \]

where \(\gamma_{\text{min}}\) is the large scale effect at the edge of the cell and \(p_{\text{max}}\) is the maximum allowable power for each MTD. Then, the average received SNR corresponding to the \(n\)-th MTD is given by

\[ \text{SNR}_n = \frac{p_{\text{max}} \gamma_{\text{min}}}{\sigma^2}. \]

With a similar analogy, the average received SNR for the \(e\)-th eMBB device is given by

\[ \text{SNR}_e = \frac{\rho_{\text{max}} \beta_{\text{min}}}{\sigma^2}. \]

The numerical results are obtained over \(10^3\) channel realizations. A summary of simulation parameters is provided in Table III.

B. Performance Metrics

To evaluate the eMBB performance achieved under the proposed solutions, we analyze the average outage probability of the eMBB devices. We mimic a practical procedure by assuming that an \(e\)-th eMBB device is successfully decoded if \(\Gamma_e\) is greater than a certain threshold [60]. We define this threshold as \(2^r - 1\), where

\[ r = \frac{b}{(T - L)T_s}. \]

is the transmit data rate in bits per channel use (bpcu), \(b\) and \(T_s\) are the number of bits and symbol time, respectively. Therefore, the average outage probability\(^{10}\) of the eMBB devices is defined by

\[ P_{out} = \Pr(\Gamma_e < 2^r - 1). \]

For the MTC network, we use the receiver operating characteristics (ROC) to quantify the inherent trade-offs related to the probability of miss detection (PMD) and probability of false alarm (PFA). It is worth highlighting that PMD and PFA are computed at the sequence level. For example PMD is the probability of missing a message rather than an active MTD as conventionally done in computing ROC [8]. Numerically, the PMD and PFA are respectively computed as

\[ \text{PMD} = \mathbb{E} \left( \frac{\sum_{i=1}^{NQ} \max(0, \alpha_i - \hat{\alpha}_i)}{|K|} \right), \]

\[ \text{PFA} = \mathbb{E} \left( \frac{\sum_{i=1}^{NQ} \max(0, \hat{\alpha}_i - \alpha_i)}{NQ - |K|} \right). \]

We also evaluate the normalized mean squared error (NMSE) of the channel estimates. This measures the relative error in the channel estimate and hence defined for the eMBB devices and MTDs as

\[ \text{NMSE}_i = \mathbb{E}_i \left( \frac{\| h_i - \hat{h}_i \|^2}{\| h_i \|^2} \right), i \in E \cup K. \]

Even though non-coherent detection does not require explicit CSI, we found it necessary to reveal the explicit performance of the SSR algorithms in the identification of the non-zero rows of \(X\) by using (37). This serves as a litmus test because performance achieved using this metric is not subject to external settings. On the other hand, detection and decoding evaluated by PMD and PFA are normally subject to how well a threshold is set.

\(^{10}\)Given that the eMBB devices are exposed to similar conditions, their average outage probability is the same as for one eMBB device.
for different
L
nel estimate performance as a function of the average SNR and presence of MTC traffic. Specifically, Fig. 4(a) shows the chan-
C. Performance of the eMBB

Fig. 4 shows the performance of the eMBB devices in the presence of MTC traffic. Specifically, Fig. 4(a) shows the channel estimate performance as a function of the average SNR and the pilot length. We have used Gaussian pilot sequences [8], [20], [21], [22] as a benchmark to show the superiority of our proposed framework. On average, results evince that increasing both the average SNR (by increasing \( \rho_r \)) and pilot lengths of the eMBB devices improves performance. These results are expected since an increase in pilot length corresponds to longer training, which reduces estimation errors. Similarly, higher transmission powers encourage predominance of the signal over low power interference and noise, thus, improving performance. A superficial analysis of these results can give the impression that longer pilot length (for the eMBB devices) guarantee a favourable coexistence with the MTDs. However, it can be quite the opposite. To assess this, Fig. 4(b) shows the average outage probability of the eMBB devices as a function of the activation probabilities (\( \epsilon \)) of the MTDs and the pilot lengths of the eMBB devices. For fixed \( L \), it is observable that higher outage probability occurs with \( \epsilon = 0.1 \) than with \( \epsilon = 0.01 \). Also, it can be noted that for fixed \( \epsilon = 0.1 \), the outage probability is higher for \( L = 128 \) than for \( L = 16 \). It is apparent that these two factors, i.e., increased activity and increased pilot lengths negatively impact the network performance by increasing the outage probability of the eMBB devices. Their impact can be interpreted using the necessary condition for decoding data from eMBB devices as detailed in (35). Explicitly, we note that an increased \( \epsilon \) probabilistically increases \(|K|\), which increases interference and thus reduces the SINR (\( \Gamma_e \)). Similarly, increasing \( L \) leads to a higher transmission rate (\( r \)) and thus increases the threshold required for successfully decoding eMBB signals. Nevertheless, both lead to the violation of the required condition to successfully decode the data sent by eMBB devices. In turn, this reduces the SIC capability, which results in the eMBB signals causing stronger interference to the MTDs during the SSR phase. It is worth noting that such strong interference reduces the BS’ ability to decode data from the MTDs, as will be seen next. For the remainder of this work, we only present results using the proposed pilot sequences as it performs better than the benchmark.

D. Performance of the MTDs

Fig. 5 shows the performance of decoding the MTDs in terms of the NMSE as a function of the average SNR and activation probability (\( \epsilon \)). In all the cases, we observe that the NMSE starts decreasing with increasing SNR until reaching a point of inflection where the NMSE starts to increase. The inflection reveals the optimal point where messages from MTDs are successfully decoded using the SSR techniques. Consequently, this point is also an optimal point for favorable coexistence between MTDs and eMBB devices. It is also important to observe that the position of this point is influenced by both average SNR values and \( \epsilon \). It can also be observed that EM-SBL and AMP generally have equal performance in low average SNR regimes and also outperform OMP and \( \ell_{2,1} \)-ADMM due to the fact that they exploit more information from the measurements. In spite of that, it can be observed that AMP is more sensitive to the system configuration, which is consistent with the discussions pointed out by the authors in [38].

In connection with our discussions in Section VI-C, high values of average SNR of the MTDs and \( \epsilon \) increase the amount of interference to the eMBB signals, which leads to higher \( P_{out} \) of the eMBB devices and failure to perform SIC. One of the interesting aspects of these results is that as \( \epsilon \) increases, smaller values of average SNR of the MTC signals are preferred for a favourable coexistence. Unfortunately, reducing average SNR values of the MTDs leads to difficulty in decoding their data, which is generally undesirable. However, it is important to note that these results show that the proposed framework enables coexistence of the different services under certain configurations. To substantiate this, we subsequently present the ROC, hence showing inherent trade-offs between PMD and PFA based on the average SNR values and outage probabilities of the eMBB devices.

Fig. 6 shows ROC performance of AMP\(^{11}\) with different average SNR values of the eMBB signals. The ROC curves in Fig. 6 can be used as a guide when choosing regions of operation for both MTDs and eMBB devices. To be explicit, we have included both the SNR levels of the eMBB devices hand in hand with the average outage probability for operating with these SNR values. It can be observed that the data from

\(^{11}\)The ROC of AMP in this region of operation is similar to that of EM-SBL, hence we only present these results.
MTDs is decoded more accurately when SNR_{e} = -60 dB than when it is -20 dB. This can be attributed to the fact that eMBB signals with average SNR of -60 dB do not cause significant interference to the MTDs and hence data from the MTDs can be decoded successfully. In spite of this (successful decoding), the average outage probability of the eMBB devices is high, as shown in Fig. 4(b), thus rendering the coexistence unfavourable. However, operating eMBB devices at SNR_{e} = -20 dB degrades detection capabilities because this average SNR value does not guarantee that eMBB devices can be decoded yet causing significant interference to signals from the MTDs. At first instant, it can be inferred that as the average SNR of eMBB devices increases, their interference to the MTDs will be stronger and that the ability to decode data from the MTDs will degrade. Contrary to this line of analysis, it can be observed that operating eMBB devices with average SNR of -10 dB leads to an improved ability to decode the MTC signals as compared to when operating with -20 dB. This is so because average SNR of -10 dB guarantees that eMBB devices are decoded with high probability which makes it possible to perform SIC. Similarly, it can be observed that when eMBB devices are operated at 30 dB, the performance approaches that achieved when operating eMBB devices at -60 dB. Intuitively, at average SNR of 30 dB, there is little performance degradation in the detection of the MTDs data, although herein both eMBB and MTC are satisfactorily coexisting. These results confirm that the proposed joint coherent and non-coherent signal processing techniques come in handy in facilitating the coexistence of the diverse services in a 5GB network.

Fig. 5 shows the ROC results for different pilot lengths of the eMBB devices. It is worth noting that due to non-coherent detection of the MTC signals, the size of Y \in \mathbb{C}^{T \times M} remains unchanged and hence the under-sampling ratio^{12} also remains the same. From the results, it is clear that the BS' ability to decode the MTC signals degrades dismally with L = 8 and L = 128, while the performance improves with L = 64. Consistent with Fig. 4(b), L = 128 comes with high outage probability of the eMBB devices, which degrades the ability to decode the data from the MTDs. Intuitively, under the current configuration, our results show that there is favourable coexistence with an intermediate values of L = 32 and L = 64. Therefore, it is important to note that while an increase in pilot length provides absolute gains in works such as [8], [21], the situation is quite different in heterogeneous networks. These results confirm the need for our proposed framework.

Fig. 8 shows the PMD (of all the SSR algorithms) as a function of M and L, for PFA = 10^{-3}. In general, it can be observed that for both L = 32 and L = 64, the PMD tends to decrease with the number of antennas at the BS. This improvement can be attributed to the fact that more antennas lead to increased diversity, which improves \Gamma_{e} and also improves performance of the SSR algorithms [8]. From the figure it can also be noted that in general EM-SBL outperforms the other SSR algorithms. Next, we present the results from varying the size of the codebook for each MTD.

^{12}Under-sampling ratio measures the number of measurements for a given vector length, e.g., \frac{T}{NQ} means that there are T available measurements to recover a vector of length NQ. Thus, a lower under-sampling ratio imposes a highly under-determined system.
collision probability makes it difficult to identify the MTDs. It is therefore necessary to note that, to facilitate coexistence between eMBB and MTC, there are some key trade-offs that have to be made, particularly, by limiting the number of eMBB devices.

VII. CONCLUSION AND FUTURE DIRECTIONS

We proposed a novel framework that enables the coexistence of heterogeneous services, thus, promising for addressing the spectrum scarcity problems in future cellular networks. Specifically, joint eMBB pilot and sensing matrix design was introduced. In this joint design, part of the sensing matrix is made orthogonal to the pilot sequences of the eMBB devices, hence permitting training without interference. We found that our framework facilitates favourable coexistence with properly configured average SNR levels for both the eMBB devices and the MTDs. Similarly, the coexistence is also highly dependent on properly selecting the pilot length for the eMBB signals, while taking into consideration the activation probability of the MTDs. Furthermore, our work revealed that increasing the number of antennas improves coexistence of services, which constitutes a key advantage of MIMO systems. Our work has, therefore, laid a foundation for a joint coherent and non-coherent signal processing framework, which can be of practical interest.

In spite of the observed promising results, the applicability of the proposed solutions can be improved by deriving optimal points of operation in terms of pilot lengths and average SNR from information theoretic perspectives. In addition, the present work assumes that active MTDs remain in that state for the whole coherence interval and as such assuming time-slotted activity. Future works can consider non-time-slotted (asynchronous) activity detection of MTDs in the coherence interval, thus improving the applicability of the proposed framework. Moreover, the current work can be extended to more general channel models such as Rician fading models.

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