Amplitude analysis of 
$D^0 \to \pi^+ \pi^- \pi^+ \pi^-$ decays using 
CLEO-c data

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Abstract
The resonant substructure of the decay $D^0 \to \pi^+ \pi^- \pi^+ \pi^-$ is studied by performing a full five-dimensional amplitude analysis. Preliminary results based on data collected by the CLEO-c detector are presented. This is the largest dataset of $D^0 \to \pi^+ \pi^- \pi^+ \pi^-$ decays analysed in this way to-date. The two most significant contributions are $D^0 \to a_1 (1260)^+ \pi^-$ and $D^0 \to \rho (770)^0 \rho (770)^0$. The line shape, mass and width of the $a_1 (1260)$ resonance are determined, and model-independent studies of the line shapes of several resonant contributions are preformed.

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1 Introduction

We present preliminary results of the amplitude analysis of the decay \(D^0 \to \pi^+\pi^-\pi^+\pi^-\). This is an independent analysis using the CLEO-c legacy dataset. The decay mode \(D^0 \to \pi^+\pi^-\pi^+\pi^-\) has the potential to make an important contribution to the determination of the \(CP\)-violating phase \(\gamma/\phi_3 \equiv -\arg(V_{ud}V_{ub}^*/V_{cd}V_{cb}^*)\) in \(B^- \to DK^-\) decays \[1, 2\]. The all-charged final state (impossible in three-body decays of \(D^0\)) particularly suits the environment of hadron collider experiments, such as LHCb. The sensitivity to the weak phase can be significantly improved with a measured amplitude model, either to be used directly in the \(\gamma\) extraction, or in order to optimise model-independent approaches \[1, 3, 4, 5\]. A study of the rich resonance structure of this four-body mode is also of considerable interest in its own right providing valuable insights into strong interactions at low energies.

2 Event Selection

The data set consists of \(e^+e^-\) collisions produced by the Cornell Electron Storage Ring (CESR) at \(\sqrt{s} \approx 3.77\,\text{GeV}\) corresponding to an integrated luminosity of \(818\,\text{pb}^{-1}\) and collected with the CLEO-c detector. At CLEO-c, \(D\) mesons are created in the process \(e^+e^- \to \psi(3770) \to D\bar{D}\), where \(D\bar{D} = D^0\bar{D}^0\) or \(D^+D^-\). We select events where one neutral \(D\) meson decays into four pions. Signal selection is performed by using the standard CLEO-c selection criteria as described in Ref. \[6\] on the candidate tracks. We reject candidates consistent with a \(D^0 \to K_S^0(\to \pi^+\pi^-)\pi^+\pi^-\) decay by requiring \(|m(\pi^+\pi^-) - m_{K_S^0}| > 7.5\,\text{MeV}\) for any \(\pi^+\pi^-\) combination. The flavour of the initial \(D\) mesons (\(D^0\) or \(\bar{D}^0\)) is determined by identifying individual charged kaons from the accompanying \(D\) decay. Assuming these kaons are the result of Cabbibo-favoured \(D\) meson decays, the flavour of both \(D\) mesons can be inferred with a mistag probability of \(\omega = (4.5 \pm 0.5)\%\) \[7\]. The number of signal events that pass the selection is \(7536 \pm 74\).

3 Amplitude analysis

An amplitude analysis is performed in order to isolate the various intermediate states contributing to the decay \(D^0 \to \pi^+\pi^-\pi^+\pi^-\). We use the isobar approach which assumes that a multi-body process can be factorized into subsequent quasi-two-body decays \[8\]. In this model, the intermediate state amplitudes can be parameterized as a product of form factors, \(B_L\), included for each vertex of the decay tree, Breit-Wigner propagators, \(T_R\), included for each resonance, \(R\), and an overall angular distribution represented by a spin factor, \(S\),

\[A_i = B_{LD} [B_{LR_1} T_{R_1}] [B_{LR_2} T_{R_2}] S_i.\]  

(1)

For \(B_L\) we use Blatt-Weisskopf damping factors \[9\] which depend on the relative orbital angular momentum, \(L\), among the daughter particles. The spin factors are constructed in a covariant tensor formalism \[10, 11, 12\]. The total amplitude for the \(D^0 \to \pi^+\pi^-\pi^+\pi^-\)
decay is given by the coherent sum over all intermediate state amplitudes weighted by the complex coefficients \(a_i\) to be measured from data:

\[
A_{D^0} = \sum_i a_i \mathcal{A}_i.
\]  

(2)

Similarly, the amplitude for \(D^0\) decays is given by \(A_{D^0} = \sum_i a_i \mathcal{A}_i\). In our default fit, we assume that there is no \(CP\) violation in this decay channel such that the amplitude coefficients for \(D\) and \(\bar{D}\) decays are identical \((a_i = \bar{a}_i)\). This assumption is tested in Sec. 6.

As the \(\pi^+\pi^-\pi^+\pi^-\) final state involves two pairs of indistinguishable pions, the amplitudes are Bose-symmetrized.

### 4 Signal model selection

The large amount of possible sub-processes in a four-body decay necessitates a model-building procedure in order to select the most significant contributions. Start with a large pool of amplitudes and use the Least Absolute Shrinkage and Selection Operator (LASSO [13]) approach to limit the model complexity, as proposed in Ref. [14]. In this method, the likelihood function is extended by a penalty term

\[
-2 \log L + \lambda \sum_i \sqrt{\int |a_i \mathcal{A}_i|^2 \, d\Phi_4},
\]  

(3)

where the integral is over the phase-space of the decay. The LASSO term shrinks the amplitude coefficients towards zero. The amount of shrinkage is controlled by the parameter \(\lambda\) to be tuned on data. Higher values for \(\lambda\) encourage sparse models, i.e. models with only a few non-zero amplitude coefficients. The optimal value for \(\lambda\) is found by minimizing the Bayesian information criteria (BIC [15]),

\[
\text{BIC}(\lambda) = -2 \log L + r \log N_{\text{sig}},
\]  

(4)

where \(N_{\text{sig}}\) is the number of signal events and \(r\) is the number of amplitudes with a decay fraction above a certain threshold. In this way, the optimal \(\lambda\) balances the fit quality \((-2 \log L)\) against the model complexity. Figure 1 shows the distribution of BIC values obtained by scanning over \(\lambda\) where we choose the threshold to be 0.5%. The set of amplitudes selected using the optimal value for \(\lambda\), which is found to be \(\lambda = 20\), is henceforth called the LASSO model.
5 Results

Table 1 lists the real and imaginary part of the complex amplitude coefficients $a_i$ obtained by fitting the LASSO model to the data, along with the corresponding fit fractions. The latter are defined as

$$F_j = \frac{\int |a_j A_j|^2 \ d\Phi_4}{\int |A_{D0}|^2 \ d\Phi_4},$$

(5)

These fractions do not have to sum to 100% due to interference. The dominant contribution is the $a_1(1260)$ resonance in the decay modes $a_1(1260) \rightarrow \rho(770)\pi$ and $a_1(1260) \rightarrow \sigma\pi$ followed by the quasi-two-body decays $D \rightarrow \sigma f_0(1370)$ and $D \rightarrow \rho(770)\rho(770)$. Figure 2 shows the distributions of the phase-space observables for data superimposed by the fit projections. A reasonable agreement is observed for each distribution. In order to quantify the quality of the fit including the correlation of the phase-space variables, a $\chi^2$ value is determined by binning the data in phase-space as

$$\chi^2 = \sum_{b=1}^{N_{\text{bins}}} \frac{[N_b - N_b^{\text{exp}}]^2}{N_b^{\text{exp}}},$$

(6)

where $N_b$ is the number of data events in a given bin, $N_b^{\text{exp}}$ is the event count predicted by the fitted PDF and $N_{\text{bins}}$ is the number of bins. An adaptive binning is used to ensure sufficient statistics in each bin for a robust $\chi^2$ calculation [7]. The $\chi^2$ value divided by the number of degrees of freedom amounts to $\chi^2/\nu = 1.33$, indicating a good fit quality.

As a cross-check, we verify the resonant phase motion of the observed $a_1(1260)$, $\pi(1300)$ and $a_1(1640)$ resonances in a quasi-model-independent way as pioneered in Ref. [16]. For this purpose, the corresponding Breit-Wigner line shapes of the resonances are replaced, one at a time, by a complex-valued cubic spline. The interpolated cubic spline has to pass
through six independent complex knots spaced in the $m^2(\pi^+\pi^+\pi^-)$ region around the nominal resonance mass. The fitted real and imaginary parts of the knots are shown in Fig. 3, where the expectations from a Breit-Wigner shape with the mass and width from the nominal fit are superimposed taking only the uncertainties on the mass and width into account. In each case, the Argand diagram shows a clear circular, counter-clockwise trajectory which is the expected behavior of a resonance. Since the investigated resonances are all very broad, the model independent line shapes can absorb statistical fluctuations in the data, especially near the phase-space boundaries. Therefore, the agreement with the Breit-Wigner expectation can be considered as qualitatively reasonable in all cases indicating that these resonances are indeed real features of the data. Finally, the fractional $CP$-even content,

$$F_+^{4\pi} = \frac{\int |A_{D^0} + A_{D^0}'|^2 \, d\Phi_4}{\int |A_{D^0} + A_{D^0}'|^2 \, d\Phi_4 + \int |A_{D^0} - A_{D^0}'|^2 \, d\Phi_4}$$  \hspace{1cm} (7)$$

is calculated from the LASSO model to be

$$F_+^{4\pi}(\text{flavour – tagged, model – dependent}) = (73.5 \pm 0.9 \, \text{(stat)})\%$$  \hspace{1cm} (8)$$

in excellent agreement with a previous model-independent analysis of $CP$-tagged events [17],

$$F_+^{4\pi}(\text{CP – tagged, model – independent}) = (73.7 \pm 2.8)\%.$$  \hspace{1cm} (9)$$

6 Search for direct $CP$ violation

A search for $CP$ violation is performed by fitting the baseline model to the flavour tagged $D^0$ and $\bar{D}^0$ samples. In contrast to our default fit described in Sec. 3, we now allow the amplitude coefficients for $D^0 \to \pi^+\pi^-\pi^+\pi^-$ and $\bar{D}^0 \to \pi^+\pi^-\pi^+\pi^-$ decays to differ. The fit to the $D^0$ and $\bar{D}^0$ samples has to be performed simultaneously in order to correctly account for mistagged events. Table 2 compares the resulting fit fractions for the $D^0$ and $\bar{D}^0$ decays. For each amplitude the direct $CP$ asymmetry,

$$A_i^{CP} = \frac{F_i - \bar{F}_i}{F_i + \bar{F}_i}$$  \hspace{1cm} (10)$$

is calculated from these fit fractions. The sensitivity to $A_i^{CP}$ is at the level of 3% to 34% depending on the decay mode. No significant $CP$ violation is observed for any of the amplitudes.
Figure 2: Invariant mass distributions of signal events (points with error bars) and fit projections (red solid line).
Table 1: Real and imaginary part of the complex amplitude coefficients and fractional contribution of each component of the LASSO model. The individual amplitudes are renormalized prior to the amplitude fit such that \( \int |A_i|^2 \, d\Phi_4 = 1 \). The quoted uncertainties are statistical only.

| Decay mode | Re \( a_i \) | Im \( a_i \) | \( F_i(\%) \) |
|------------|--------------|--------------|-------------|
| \( D^0 \to \pi^- \ [a_1(1260)^+ \to \pi^- \rho(770)] \) | 100.0 (fixed) | 0.0 (fixed) | 36.7 ± 2.4 |
| \( D^0 \to \pi^- \ [a_1(1260)^+ \to \pi^- \sigma] \) | 43.8 ± 4.5 | 35.5 ± 4.2 | 10.9 ± 1.5 |
| \( D^0 \to \pi^+ \ [a_1(1260)^- \to \pi^+ \rho(770)] \) | 31.9 ± 3.7 | 10.7 ± 2.8 | 4.1 ± 0.5 |
| \( D^0 \to \pi^- \ [a_1(1260)^- \to \pi^- \sigma] \) | 10.2 ± 2.3 | 16.2 ± 2.2 | 1.2 ± 0.2 |
| \( D^0 \to \pi^- \ [\pi(1300)^+ \to \pi^- (\pi^+ \pi^-)\rho] \) | −17.2 ± 2.7 | −37.3 ± 5.0 | 6.1 ± 0.7 |
| \( D^0 \to \pi^- \ [\pi(1300)^+ \to \pi^- \sigma] \) | −33.4 ± 4.4 | 5.6 ± 3.5 | 4.2 ± 1.0 |
| \( D^0 \to \pi^+ \ [\pi(1300)^- \to \pi^+ (\pi^+ \pi^-)\rho] \) | −25.4 ± 4.4 | 2.8 ± 4.6 | 2.3 ± 0.5 |
| \( D^0 \to \pi^- \ [\pi(1300)^- \to \pi^- \sigma] \) | −3.2 ± 4.3 | 20.6 ± 3.4 | 1.6 ± 0.4 |
| \( D^0 \to \pi^- \ [a_1(1640)^- [D] \to \pi^- \rho(770)] \) | −16.2 ± 4.5 | 28.1 ± 8.9 | 3.6 ± 0.6 |
| \( D^0 \to \pi^- \ [a_1(1640)^- \to \pi^- \sigma] \) | 0.1 ± 0.4 | −18.3 ± 5.1 | 1.2 ± 0.5 |
| \( D^0 \to \pi^- \ [\pi_2(1670)^+ \to \pi^+ f_2(1270)] \) | 0.2 ± 2.6 | 21.0 ± 2.7 | 1.5 ± 0.3 |
| \( D^0 \to \pi^- \ [\pi_2(1670)^+ \to \pi^- \sigma] \) | −15.0 ± 2.7 | −27.1 ± 3.5 | 3.3 ± 0.6 |
| \( D^0 \to \sigma f_0(1370) \) | 28.3 ± 3.4 | 69.8 ± 5.9 | 18.4 ± 1.4 |
| \( D^0 \to \sigma \rho(770) \) | 34.8 ± 4.4 | −9.5 ± 4.0 | 4.4 ± 1.0 |
| \( D^0 \to \rho(770) \rho(770) \) | 1.0 ± 3.0 | 15.1 ± 3.7 | 0.9 ± 0.3 |
| \( D^0[P] \to \rho(770) \rho(770) \) | −4.1 ± 2.7 | −41.6 ± 2.6 | 7.1 ± 0.5 |
| \( D^0[D] \to \rho(770) \rho(770) \) | −66.4 ± 5.1 | 0.1 ± 3.1 | 15.5 ± 1.2 |
| \( D^0 \to f_2(1270) f_2(1270) \) | −7.9 ± 2.5 | −15.4 ± 2.3 | 1.1 ± 0.3 |

Sum

\[ \chi^2/\nu \]

\[ 1.33 \]

\[ F^{\text{fit}}(\%) \]

\[ 73.5 ± 0.9 \]

Figure 3: Argand diagrams of the quasi-model-independent \( a_1(1260) \) (left), \( \pi(1300) \) (middle) and \( \pi(1640) \) (right) line shapes. In each case, the fitted knots are displayed as points with error bars and the black line shows the interpolated spline. The Breit-Wigner line shape with the mass and width from the nominal fit is superimposed (red area). The latter is chosen to agree with the interpolated spline at the point Re\( (A) = 1 \), Im\( (A) = 0 \).
| Decay mode                              | $F_1(\%)$  | $F_2(\%)$  | $A_{CP}[\%]$ |
|----------------------------------------|------------|------------|---------------|
| $D^0 \rightarrow \pi^- [a_1(1260)^+ \rightarrow \pi^+ \rho(770)]$ | 38.8 ± 2.5 | 35.2 ± 2.4 | 5.0 ± 3.2     |
| $D^0 \rightarrow \pi^- [a_1(1260)^+ \rightarrow \pi^+ \sigma]$ | 10.9 ± 1.5 | 9.9 ± 1.3  | 5.0 ± 3.2     |
| $D^0 \rightarrow \pi^+ [a_1(1260)^- \rightarrow \pi^- \rho(770)]$ | 4.4 ± 0.8  | 3.9 ± 0.8  | 6.8 ± 13.2    |
| $D^0 \rightarrow \pi^+ [a_1(1260)^- \rightarrow \pi^- \sigma]$ | 1.2 ± 0.3  | 1.1 ± 0.3  | 6.8 ± 13.2    |
| $D^0 \rightarrow \pi^- [\pi(1300)^+ \rightarrow \pi^+ (\pi^+ \pi^-)\rho]$ | 5.8 ± 0.9  | 6.8 ± 1.0  | -7.4 ± 8.0    |
| $D^0 \rightarrow \pi^- [\pi(1300)^+ \rightarrow \pi^+ \sigma]$ | 4.5 ± 0.7  | 5.2 ± 0.8  | -7.4 ± 8.0    |
| $D^0 \rightarrow \pi^+ [\pi(1300)^- \rightarrow \pi^- (\pi^+ \pi^-)\rho]$ | 1.9 ± 0.5  | 2.3 ± 0.6  | -9.6 ± 16.5   |
| $D^0 \rightarrow \pi^+ [\pi(1300)^- \rightarrow \pi^- \sigma]$ | 1.5 ± 0.4  | 1.8 ± 0.5  | -9.6 ± 16.5   |
| $D^0 \rightarrow \pi^- [a_1(1640)^+ [D] \rightarrow \pi^+ \rho(770)]$ | 3.6 ± 0.7  | 3.1 ± 0.7  | 7.8 ± 12.5    |
| $D^0 \rightarrow \pi^- [a_1(1640)^+ \rightarrow \pi^+ \sigma]$ | 1.2 ± 0.5  | 1.0 ± 0.5  | 7.8 ± 12.5    |
| $D^0 \rightarrow \pi^- [\pi_2(1670)^+ \rightarrow \pi^+ f_2(1270)]$ | 1.8 ± 0.5  | 1.6 ± 0.5  | 6.7 ± 14.0    |
| $D^0 \rightarrow \pi^+ [\pi_2(1670)^+ \rightarrow \pi^+ \sigma]$ | 3.3 ± 0.8  | 2.9 ± 0.6  | 6.7 ± 14.0    |
| $D^0 \rightarrow \sigma f_0(1370)$ | 16.9 ± 1.6 | 20.2 ± 1.5 | -8.7 ± 4.5    |
| $D^0 \rightarrow \sigma \rho(770)$ | 6.4 ± 1.4  | 3.8 ± 1.1  | 26.3 ± 15.2   |
| $D^0 \rightarrow \rho(770) \rho(770)$ | 0.5 ± 0.4  | 1.3 ± 0.6  | -46.7 ± 34.0  |
| $D^0[P] \rightarrow \rho(770) \rho(770)$ | 6.5 ± 0.6  | 7.8 ± 0.7  | -9.1 ± 7.9    |
| $D^0[D] \rightarrow \rho(770) \rho(770)$ | 13.9 ± 1.7 | 16.3 ± 2.1 | -7.9 ± 8.3    |
| $D^0 \rightarrow f_2(1270) f_2(1270)$ | 0.9 ± 0.4  | 1.6 ± 0.5  | -28.7 ± 20.7  |

Table 2: Fit fractions for $D^0$ and $\bar{D}^0$ decays along with the $A_{CP}$ values. Only the statistical uncertainties are given.
7 Conclusions

Preliminary results from the first amplitude analysis of flavor-tagged $D \rightarrow \pi^+\pi^-\pi^+\pi^-$ decays have been presented. The study uses $e^+e^-$ collision data produced at the $\psi(3770)$ resonance corresponding to an integrated luminosity of $818 \text{ pb}^{-1}$ and recorded by the CLEO-c detector. Due to the large amount of possible intermediate resonance components, a model-building procedure has been applied which balances the fit quality against the number of free fit parameters. The selected amplitude model contains a total of 18 components. The prominent contribution is found to be the $a_1(1260)$ resonance in the decay modes $a_1(1260) \rightarrow \rho(770)\pi$ and $a_1(1260) \rightarrow \sigma\pi$. Further cascade decays involve the resonances $\pi(1300)$ and $a_1(1640)$. Their line shapes have been studied in a model-independent approach and found to be consistent with the Breit-Wigner prediction. The $CP$-even fraction of the decay $D \rightarrow \pi^+\pi^-\pi^+\pi^-$ as predicted by the amplitude model is in excellent agreement with a previous model-independent study providing an important cross-check of the model. The amplitude model has also been used to search for $CP$ violation in $D_0^0 \rightarrow \pi^+\pi^-\pi^+\pi^-$ and $\overline{D}_0^0 \rightarrow \pi^+\pi^-\pi^+\pi^-$ decays. No $CP$ violation among the amplitudes is observed within the given precision of a few percent.

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