Hybrid Parallel Computation of Integration in GRACE

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Abstract

With an integrated software package GRACE, it is possible to generate Feynman diagrams, calculate the total cross section and generate physics events automatically. We outline the hybrid method of parallel computation of the multi-dimensional integration of GRACE. We used MPI (Message Passing Interface) as the parallel library and, to improve the performance we embedded the mechanism of the dynamic load balancing. The reduction rate of the practical execution time was studied.
1 Introduction

The requirements for reducing the practical execution time in GRACE have fostered our interest in parallelization of the multi-dimensional integration of GRACE. In addition, reducing the program size becomes more important to avoid the cash-miss, which increases the practical execution time, as the number of final particles becomes large. These motivations have lead to implement the parallelization of GRACE.

In GRACE, for the multi-dimensional integration, BASES/SPRING is used. BASES is a software package of Monte Carlo integration with an importance and stratified sampling method. For the parallelization of Monte Carlo integration, it is natural and efficient to distribute sampling points to processors. This parallelization is called the Data Parallel. When the integrand can be decomposed, the Function Parallel is applicable, that is, each part of the integrand is calculated in each different processor. Since 1992, we have investigated independently these two approaches to the parallel computation of the multi-dimensional integration in GRACE.

Based on above experiences, we have developed a new method, a hybrid use of Data Parallelism and Function Parallelism. In this method, we use MPI-1 as the Message Passing Library which is standardized and is widely used for developing parallel code in both the distributed computing environment and MPP (Massively Parallel Processors) platform. A computing model adopted is SPMD (Single Program Multiple Data) computing model.

In this paper, in section 2 the details of the implementation of hybrid use of Data Parallelism and Function Parallelism is described. We also present the mechanism of the dynamic load balancing in section 3. The behavior of performance of the parallel computation is shown in section 4. Section 5 is devoted to a conclusion.

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1 The first version of MPI standard. It is standardized in May 1994.
2 Hybrid Use of Data and Function Parallelism

In the hybrid method, we firstly distribute a group of hypercubes which are subspaces of the integral volume. In each hypercube, a definite number of sampling points are taken. The distribution of hypercubes corresponds to the distribution of sampling points. Secondly, together with distributing sampling points, we distribute the calculation of the scattering amplitudes, of which the integrand consists. The scattering amplitude is given as a sum of each matrix element corresponding to each Feynman diagram. Therefore the distribution of the calculation of the scattering amplitudes corresponds to distribution Feynman diagrams.

For the data-transfer among processors, we use a collective communication instead of the point-to-point communication. The collective communication is defined in a communicator which is one of the important concepts in MPI. It defines the communication space used for the communications among processors.

Fig. 1 shows the schematic view how the Data Parallel and the Function Parallel work together from the point of view of communicators, where hypercubes, as an example, are divided into two groups (DP1 and DP2) and then calculation of Feynman diagrams into three groups (FP1, FP2 and FP3). The communicator corresponding to the Data Parallelism is indicated as dpcom. On the other hand, the communicator corresponding to the Function Parallelism is indicated as fpcom. In fpcom, the global sum of the results of the calculation of the scattering amplitudes from each processor is carried out. Successively, in dpcom the global sum of several results needed for estimating the integral is carried out. In the figure, note that dpcom (hatched in the figure) is constructed by one of PE’s (Processing Elements) in each group, DP1 and DP2, to avoid making a global sum repeatedly.

Also note that the total number of parallel processors is given as the product of the degree of the Data Parallel and that of the Function Parallel. In this example, the number of parallel processors is $2 \times 3 = 6$.

Summarizing, the parallel computation of the multi-dimensional integration is proceeded in the following way:

1. distribute hypercubes into parallel processors,
2. by using sampling points in hypercubes distributed, calculate a part of integrand (scattering amplitudes) in each parallel proces-
Figure 1: Schematic view of *Communicators*. PE#n represents each parallel processor. DP1 and DP2 are groups defined for distributing *hypercubes*. FP1, FP2 and FP3 are groups for distributing Feynman diagrams. dpcom and fpcoms represent the *communicator* for the Data Parallel and for the Function Parallel, respectively. MPI_COMM_WORLD is a predefined *communicator* by MPI.
3. make a global sum of the scattering amplitudes for each sampling point in the communicator fpcom.

4. square the results obtained in (iii) and sum them up in the group, DP1 and DP2,

5. make a global sum in the communicator dpcom.

The above procedures are iterated until the multi-dimensional integration converges.

3 Dynamic Load Balancing

Once a physics process to be calculated is fixed, GRACE generates the Feynman diagrams according to defined physics model and defined order of the perturbation. Generated diagrams are numbered by GRACE for convenience. Assuming all these diagrams have the same numbers of vertices and internal lines for simplicity, the execution time needed to calculate each diagram is expected to be nearly identical. On this assumption, we distributed Feynman diagrams into parallel processors in the order conventionally numbered by GRACE[6, 7].

However, indeed, the execution time required for calculating each Feynman diagram varies diagram by diagram because diagrams may have different kinds of couplings and internal lines. This small fluctuation causes the load imbalance among parallel processors and leads to the decrease of the performance.

We newly add the mechanism of the dynamic load balancing. The execution time of each diagram is automatically measured in the calculation of the scattering amplitudes. As the procedures 1. - 5. described in section 2 are iterated, diagrams are sorted in order of the height of the load. With these rearrangements of diagrams, the load on each parallel processor becomes well balanced. In Fig. 2, the way how the fluctuations of the load on each processor becomes small is shown when the degree of the Function Parallel is 8 and the number of Feynman diagrams is 232.

4 Performance Measurement

The performance of the parallel computation is often represented by the scalability which is the ratio of the resultant execution time to the
Figure 2: Averaged execution time for calculating scattering amplitudes in each sampling point in each PE. A vertical axis is averaged execution time in second. A horizontal axis is the number of iterations.
Table 1: Reduction rate of the execution time with hybrid method. The figures in the columns show the behavior of the scalability with fixed degree of the Function Parallel. The figures in the rows show the behavior of the scalability with fixed degree of the Data Parallel.

| Function | 1    | 2    | 4    | 8    | 16   |
|----------|------|------|------|------|------|
| 1        | 1.00 | 1.97 | 3.97 | 8.03 | 15.82|
| 2        | 2.02 | 3.95 | 7.60 | 15.56| -    |
| 4        | 3.91 | 7.57 | 14.96| -    | -    |
| 8        | 7.15 | 13.79| -    | -    | -    |
| 16       | 12.02| -    | -    | -    | -    |

The physics process used in the measurement is:
- a physics process \(e^+e^- \rightarrow b\bar{b}d\bar{u}\nu_d\mu\), and
- the total number of Feynman diagrams involved in this physics process is 232 at a tree level with the unitary gauge.

The performance measurement has been performed on AP3000 in Fujitsu Parallel Computing Research Center in Kawasaki, Japan. The AP3000 system consists of UltraSPARC -II 300MHz processors connected via AP-Net\(^2\) providing 200MB/s bandwidth per port. Of data-transfers among processors, the results gathered in \texttt{fpcm} are the biggest and the size of them is about 8.4MB per each transfer for the above physics process. In this measurement, the number of data-transfer is 8 times.

Table I clearly shows that the parallel computation gives an excellent effect to reduce the practical execution time of the multi-dimensional integration in \texttt{GRACE}.

\(^2\)AP-Net is a two-dimensional torus network.
5 Conclusion

We implemented a hybrid method of the Data Parallel and the Function Parallel in the multi-dimensional integration of GRACE. In the parallel computation of Monte Carlo integration, not only the sampling points but also the calculations of scattering amplitudes are distributed into parallel processors. We used MPI-1 as Message Passing Library. In the hybrid method, we can set the degree of the Data Parallel and that of the Function Parallel independently. The total number of parallel processors is given as the product of these two degrees. The computing model we used is SPMD model. To reduce the load imbalance among processors due to the small fluctuations of execution time for calculating each Feynman diagram, we implemented the mechanism of the dynamic load balancing for distributing Feynman diagrams to processors. With this mechanism, the effect to the reduction of the elapsed time in GRACE has been improved.

The reduction rate of the execution time has been measured on Fujitsu AP3000 system by using up to 16 processors for the physics process $e^+e^− \rightarrow bbud\bar{\nu}_\mu\mu$. In this study, we found when the program size is not large, the Data Parallel gives better performance than the Function Parallel. When, however, the program size is large, it is impossible to run the program on a single processor. In this case, we have to take the Function Parallel. Our study tells even the Function Parallel gives satisfactory results. Further, when the network speed is enough high, it is expected that the performance by the Function Parallel becomes high as the Data Parallel.

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