Temperature log simulations in high-enthalpy boreholes

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Abstract

Temperature logs have important applications in the geothermal industry such as the estimation of the static formation temperature (SFT) and the characterization of fluid loss from a borehole. However, the temperature distribution of the wellbore relies on various factors such as wellbore flow conditions, fluid losses, well layout, heat transfer mechanics within the fluid as well as between the wellbore and the surrounding rock formation, etc. In this context, the numerical approach presented in this paper is applied to investigate the influencing parameters/uncertainties in the interpretation of borehole logging data. To this end, synthetic temperature logs representing different well operation conditions were numerically generated using our newly developed wellbore simulator. Our models account for several complex operation scenarios resulting from the requirements of high-enthalpy wells where different flow conditions, such as mud injection with- and without fluid loss and shut-in, occur in the drill string and the annulus. The simulation results reveal that free convective heat transfer plays an important role in the earlier evolution of the shut-in-time temperature; high accuracy SFT estimation is only possible when long-term shut-in measurements are used. Two other simulation scenarios for a well under injection conditions show that applying simple temperature correction methods on the non-shut-in temperature data could lead to large errors for SFT estimation even at very low injection flow rates. Furthermore, the magnitude of the temperature gradient increase depends on the flow rate, the percentage of fluid loss and the lateral heat transfer between the fluid and the rock formation. As indicated by this study, under low fluid losses (< 30%) or relatively higher flow rates (> 20 L/s), the impact of flow rate and the lateral heat transfer on the temperature gradient increase can be ignored. These results provide insights on the key factors influencing the well temperature distribution, which are important for the choice of the drilling data to estimate SFT and the design of the inverse modeling scheme in future studies to determine an accurate SFT profile for the high-enthalpy geothermal environment.

Keywords: Temperature logs, Static formation temperature, Wellbore simulation, High-temperature well, Horner-plot method, Heat transfer, Fluid loss
Introduction

Geothermal explorations depend strongly on reservoir conditions which are evaluated by increasingly sophisticated reservoir simulators (Cacace et al. 2010; O’Sullivan and O’Sullivan 2016; Konrad et al. 2019). Also, data acquisition, mostly of seismic data, has reached a high degree of complexity. This is, however, contrasted by little effort in the evaluation of logging data, especially of temperature logs. Usually, the primary objectives of running a temperature survey in a well are to obtain valuable information on geothermal reservoirs such as the static formation temperatures (SFT) and the location of fluid loss zones. This requires temperature logs measured at different stages (mud circulation and shut-in) during the evolution of the temperature in the borehole fluid-formation system as well as different interpretation techniques of these temperature logs (Witterholt and Tixier 1972).

The SFT is usually inferred from the measurement of bottom-hole temperature (BHT) when the drilling circulation has stopped and the borehole fluid temperature gradually develops towards the initial or unperturbed formation temperature. Due to the thermal disturbances caused by the drilling mud, the measured BHT is usually lower than the true SFT and needs to be corrected to obtain a reliable estimate (Deming 1989; Gotorbe et al. 2007). Various temperature correction methods based on different simplified physical models have been developed, e.g., the Horner-plot method [or constant line source method (Bullard 1947; Dowdle and Cobb 1975)]; the spherical and radial heat flow method (Ascencio et al. 1994, 2006); the Hasan-Kabir method (or conductive-convective cylindrical heat source model (Hasan and Kabir 1994) and the Kutatov–Eppelbaum method [or generalized Horner method (Kutatov and Eppelbaum 2005)]. These methods are based on linear or non-linear regression models that describe the relationship between measured BHT and time functions (Verma et al. 2006a, Verma et al. 2006b; Wong-Loya et al. 2012) accounting for the transient effects of thermal recovery during the shut-in phase of the borehole. The simplicities in these methods make them very prevalent engineering tools for estimating SFT.

Another important application of temperature logs is the identification of fluid loss or feed zones from temperature data obtained under hydraulic testing conditions (Okandan 2012; Steingrimsson 2013). Examples of using temperature measurements in boreholes are multifold. Pehme et al. (2010) identified hydraulically active fractures in dolomite and sandstone aquifers; Kleipikova et al. (2011) estimated local transmissivities and hydraulic head differences; Nian et al. (2015) predicted flow rates in oil and gas production wells. These authors stressed the satisfactory accuracy of temperature-derived flow velocities compared to direct flow measurement. In recent years, fiber-optic distributed temperate sensing (DTS), which is a robust means of acquiring continuous temperature profiles instantaneously along the length of the cable (Großwig et al. 1996), has also been extensively used to improve the accuracy of flow rate profiling and the detection of fracture zones (Read et al. 2013; Coleman et al. 2015; Read et al. 2015; Bense et al. 2016).

In a high-temperature environment, the acquisition of logging data from exploration and drilling projects in geothermal fields is more challenging compared to its petroleum counterparts. In recent years, high-temperature geothermal systems have gained attention due to their large potential for energy extraction. In fact, a number of wells drilled in geothermal fields such as The Geysers (USA), Los Humeros (Mexico), Kakkonda (Japan), Larderello
(Italy), and Reykjanes (Iceland) have been reported (Reinsch et al. 2017; Kruszewski and Wittig 2018) to even reach supercritical conditions for water ($T > 374 \, ^\circ C$, $P > 221$ bar). Reliable logging in such extreme well conditions is currently very challenging using conventional tools, which are normally rated up to 175 °C bottom-hole temperature (Baird et al. 1993). Although high temperature and pressure logging tools are available (Ikeuchi et al. 1998; Sekine et al. 2004; Reinsch et al. 2013), these tools are generally all restricted to specific operating conditions in harsh environments. For example, the electronic Kuster K10, a commonly used commercial tool in the industry, can operate at a maximum of 350 °C only up to 4 h (Danielsen 2008). This short period may be sufficient for the tripping of the logging tools but not for collecting data to resolve the transient thermal response under shut-in condition. DTS, which is considered better suited for use at elevated temperatures, gives erroneous temperature readings under high temperatures (> 300 °C) due to the chemical and thermal degradation of the optical fiber (Reinsch et al. 2013; Laarossi et al. 2019).

To keep the temperature of the measuring device below its maximum tolerance, cooling through continuous injection during logging is necessary for extreme high-temperature boreholes (Friðleifsson et al. 2018).

The present study focuses on the analysis of temperature logging data from high-temperature geothermal wells. It particularly addresses the specific conditions (e.g., drill pipe-and-annulus geometry and continuous injection) which result from the requirements of such an environment. Two sets of simulation examples are analyzed to reflect possible logging conditions in a high-enthalpy well. In the first example, fluid injection followed by shut-in is simulated. This example is used to examine the validity of applying simple BHT correction methods on the shut-in temperature data to estimate SFT, as well as to evaluate the impact of the free convection heat transfer in the build-up of borehole fluid temperature and the SFT estimation results. To the authors’ knowledge, the latter was hardly discussed in former wellbore simulation studies (Espinosa-Paredes et al. 2009; Yang et al. 2015). The second example investigates two new topics for high-temperature geothermal wells under-injection. One scope of the investigation is whether simple BHT type correction methods are still applicable to logging data from boreholes which are under continuous cooling due to the restriction of the logging tool. Furthermore, a new method is discussed to quantify the fluid loss percentage from temperature logs by computing the ratio of temperature gradient below and above the fluid loss point.

Methods

Analytical approach to estimate SFT-Horner-plot method

Herein, the Horner-plot method (HM) for SFT estimation using shut-in temperature logs is analyzed. This method was selected due to its wide application in the geothermal industry (Andaverde et al. 2005; Kutasov and Eppelbaum 2018). The evaluations of other SFT estimation methods fall outside the scope of this paper but can be achieved similarly. The HM approximates the thermal effect of the drilling as an infinitely thin and long axial heat source extracting heat at a constant rate and, therefore, perfect conducting conditions in the well are assumed. The mathematical form of the HM is simplified as follows:

$$T_s = T_i + \frac{q}{4\pi \lambda_s} \ln \frac{t_c + t_s}{t_s},$$

(1)
where $T_s$ is the borehole shut-in temperature, $T_i$ is the SFT, $t_c$ is the shut-in time, $t_c$ is the circulation time, $q$ is the heat extraction rate. According to Eq. 1, a semi-logarithmic plot of $T_s$ against the Horner dimensionless time $(t_c + t_s)/t_s$ should be a straight line intercepting with the vertical axis at $T_i$. The standard procedure of applying the Horner-plot method has been to extrapolate this line until $t_s \rightarrow \infty$ (Horner dimensionless time = 1) with the intercept yielding the SFT value.

**Numerical approach**

An in-house numerical simulation tool is used to model the thermal behavior of the wellbore and its surrounding formation. The simulator is an application developed based on the MOOSE framework which provides a multiphysics object-oriented simulation environment (Gaston et al. 2009). MOOSE allows for efficient utilization of a wide range of computational hardware using both shared-memory and distributed-memory parallelism (Permann et al. 2013). The MOOSE-based application consists of different physics modules which can be easily added, removed and coupled for solving variables in an implicit and fully coupled manner.

Figure 1 shows the schematic of typical wellbore flow and heat transfer scenarios. The cold drill fluid is considered to be either injected both in through the drill pipe and the annulus (coflow); or injected in the drill pipe and circulated back to the surface (counterflow). The simulator assumes the wellbore to be treated either as a one-dimensional or a two-dimensional structure depending on the problem being studied. When a two-dimensional wellbore structure is considered, the wellbore components, such as the fluid inside the drill pipe, the drill pipe wall, the annulus, and the casings,
are treated as different regions (region 1, 2, 3, 4, respectively) in which the temperatures \(T_1, T_2, T_3, \text{ and } T_4\) need to be solved as individual variables (Fig. 1). These variables are linked through the interfacial heat transfer relationships between the fluid and the solid. The injection fluid was assumed to be pure liquid water. Fluid properties such as density, viscosity, and heat capacity were calculated according to the IAPWS-IF97 formulation (Cooper and Dooley 2007). The fundamental assumptions of the models considered in this work are: the geometries of the wellbore and formation are cylindrical, the fluid is incompressible, fluid flow is in the axial direction only, the rock formation is impermeable, there is no radial temperature gradient within the fluid when the wellbore is considered to be a two-dimensional structure, thermal dissipation and expansion effects are negligible.

Making these assumptions, the energy conservation equation for the fluid inside the drill pipe and annulus is written in the following form:

\[
\rho_f C_{pf} \left( \frac{\partial T_f}{\partial t} + v_{zf} \frac{\partial T_f}{\partial z} + v_{rf} \frac{\partial T_f}{\partial r} \right) - \frac{\lambda_f}{r} \frac{\partial T_f}{\partial r} - \frac{\lambda_f}{r^2} \frac{\partial^2 T_f}{\partial r^2} - \frac{\lambda_f}{r^2} \frac{\partial^2 T_f}{\partial z^2} = 0
\]

(2)

The continuity equation for incompressible flow is given by:

\[
\frac{1}{r} \frac{\partial (rv_{rf})}{\partial r} + \frac{\partial v_{zf}}{\partial z} = 0,
\]

(3)

where \(\rho_f\) is the fluid density, \(C_{pf}\) is the fluid specific heat capacity, \(v_z\) and \(v_r\) are the axial and radial flow velocities, respectively, \(\lambda_f\) is the thermal conductivity.

The energy conservation equation for the pipe wall, casing and formation can be expressed as:

\[
\rho_s C_{ps} \frac{\partial T_s}{\partial t} - \frac{\lambda_s}{r} \frac{\partial T_s}{\partial r} - \frac{\lambda_s}{r^2} \frac{\partial^2 T_s}{\partial r^2} - \frac{\lambda_s}{r^2} \frac{\partial^2 T_s}{\partial z^2} = 0,
\]

(4)

where \(\rho_s, C_{ps}, \lambda_s\) is the density, heat capacity and thermal conductivity of the pipe wall, casing and formation, respectively.

The final forms of the above governing equations for regions 1, 2, 3, 4 (Fig. 1) are simplified into:

\[
\frac{\partial v_{zi}}{\partial z} = 0, \quad i = 1, 3
\]

(5)

\[
\rho C_p \left( \frac{\partial T_i}{\partial t} + v_{zi} \frac{\partial T_i}{\partial z} \right) - \frac{\lambda}{r} \frac{\partial T_i}{\partial r} - \frac{\lambda}{r^2} \frac{\partial^2 T_i}{\partial r^2} - \frac{\lambda}{r^2} \frac{\partial^2 T_i}{\partial z^2} = 0, \quad i = 1, 3
\]

(6)

\[
\rho C_p \frac{\partial T_i}{\partial t} - \frac{\lambda}{r} \frac{\partial T_i}{\partial r} - \frac{\lambda}{r^2} \frac{\partial^2 T_i}{\partial r^2} - \frac{\lambda}{r^2} \frac{\partial^2 T_i}{\partial z^2} = 0, \quad i = 2, 4
\]

(7)

where \(i\) refers to the region number.

The initial and boundary conditions of the thermal–hydraulic models considered in this work are given in Table 1. The validation of the numerical tool is done by comparing the numerical simulation results and analytical solutions of Ramey’s wellbore
As mentioned above, the thermal exchange between different wellbore regions is modeled via thermal transfer relations at their interfaces (Table 1, BC2). The heat transfer coefficient, \( h \), is the proportionality constant between the heat flux and the thermodynamic driving force for the heat flow (i.e., the temperature difference between adjacent wellbore components, \( \Delta T \)). In this work, the heat transfer coefficients under forced convection and shut-in condition are correlated and calculated using different approaches.

**Forced convection**

Under forced convection, the heat transfer coefficient is defined as (Yang et al. 2015):

\[
    h = \frac{Nu \cdot \lambda_f}{d} \quad (8)
\]

where \( Nu \) is the Nusselt number, \( d \) is the hydraulic diameter of the drill pipe and annulus.

For laminar flow inside the annulus, \( Nu \) is calculated using the Sieder–Tate correlation (Kohl et al. 2002):

\[
    Nu = 1.86(Re Pr)^{1/3} \left( \frac{d}{L} \right)^{1/3} \left( \frac{\mu}{\mu_w} \right)^{0.14}, \quad Re \leq 2300, \quad (9)
\]

where \( L \) is the length of the tube, \( Pr \) is the Prandtl number, \( \mu \) is the dynamic viscosity of the bulk fluid, \( \mu_w \) is the fluid viscosity at the temperature of the tube wall.
In the laminar regime inside the drill string

\[ \text{Nu} = 4.364, \quad \text{for} \quad \text{Re} \leq 2300 \]  \hspace{1cm} (10)

For highly turbulent flow, the Dittus–Boelter equation (Dittus and Boelter 1985) is applied:

\[ \text{Nu} = 0.023 \cdot \text{Re}^{0.8} \cdot \text{Pr}^{0.3}, \quad \text{for} \quad \text{Re} \geq 1 \times 10^4. \]  \hspace{1cm} (11)

For the transition between laminar and highly turbulent flow, the Nusselt number is estimated by the following linear interpolation (Diersch et al. 2011; Gnielinski 2013):

\[ \text{Nu} = (1 - \gamma) \cdot 4.364 + \gamma \cdot 0.023 \cdot \text{Re}^{0.8} \cdot \text{Pr}^{0.3}, \quad \text{for} \quad 2300 < \text{Re} < 1 \times 10^4 \]  \hspace{1cm} (12)

with

\[ \gamma = \frac{\text{Re} - 2300}{10^4 - 2300} \]  \hspace{1cm} (13)

**Shut-in condition**

So far in most theoretical and simulation studies, pure conductive heat flow in a static water column is assumed when estimating temperature recovery during borehole shut-in (Shen and Beck 1986; García et al. 1998; Espinosa-Paredes et al. 2001; Yang et al. 2015). The heat transfer coefficient in the borehole fluid is then approximated by:

\[ h_c = \frac{\dot{Q}_f}{\pi r_{wb}^2}, \]  \hspace{1cm} (14)

where \( r_{wb} \) is the borehole radius.

However, several studies have reported the existence of another key factor in the heat transfer, which is free convection caused by density differences arising from vertical temperature gradients (Diment 1967; Greterener 1967; Pfister and Rybach 1995; Berthold and Börner 2008; Eppelbaum and Kutasov 2011; Klepikova et al. 2018). The critical parameters for the free convection process can be indicated by the following equation (Diment and Urban 1983):

\[ \nabla T_{cr} = \frac{g \cdot \alpha \cdot T_{abs}}{c_p} + \frac{C \cdot v \cdot D_f}{g \cdot \alpha \cdot r_{wb}^4}, \]  \hspace{1cm} (15)

where \( \nabla T_{cr} \) is the critical thermal gradient to initiate free convection, \( g \) is the acceleration due to gravity, \( \alpha \) is the thermal expansion coefficient, \( T_{abs} \) is the absolute temperature (K), \( c_p \) is the specific heat capacity, \( C \) is a constant with a value of 216 for tubes, \( v \) is the fluid kinematic viscosity, \( D_f \) is the fluid thermal diffusivity. Taking the following values as typical for the borehole fluid: \( v = 1 \times 10^{-6} \text{ m}^2/\text{s}, \alpha = 2 \times 10^{-4} \text{ K}^{-1}, D_f = 1.4306 \times 10^{-7} \text{ m}^2/\text{s}, c_p = 4149 \text{ J/(kg K)} \), absolute temperature range of 273.15–573.15 K. This equation reveals that for a borehole with a radius of 35–150 mm, the average critical thermal gradient needed to initiate free convection is 2.36e−4 to 1e−2 K/m.

Unlike forced convection, which normally acts only in the axial direction, free convection enhances the heat transfer in all directions through fluid circulation and mixing. However, a well-established quantitative description of the thermal effect of free
Convection in boreholes is still missing, and a general modeling approach is not available. Luheghi (1983) showed that free convection does not significantly enhance vertical heat transfer. Since the radial temperature gradient is typically much larger, the contribution to heat flux in the vertical direction by free convection is considered negligible. However, he mentioned it might be necessary to account for the enhancement in radial heat flux due to the mixing effect of fluid motion induced by buoyancy forces. In our work, we have assumed the increase of the heat transfer rate due to free convection only acts in the radial direction. The overall heat transfer coefficient can be written as:

\[ h = h_c + h_{\text{free}}, \] (16)

which means that the heat transfer for the shut-in condition results from conduction and free convection.

In our models, the heat transfer coefficient for forced convection was calculated explicitly according to Eqs. (8)–(13). While for the shut-in condition, the heat transfer due to free convection was either neglected \( h_{\text{free}} = 0 \) or was implicitly evaluated (e.g. \( h_{\text{free}} \) is a factor or fraction of \( h_c \)).

**Simulation scenarios**

In the simulation studies, we began with the application of HM to the simulated shut-in temperature logs. Then we simulated two logging scenarios in a high-temperature environment. In one scenario, temperature logs obtained under continuous borehole cooling were used to estimate SFT and the sensitivity of the estimation error to different flow rates was investigated. In another scenario, temperature logs were used to quantify the fluid loss in the well.

**Shut-in temperature logs simulation**

The evaluation of the HM was conducted by numerical simulation of both the circulation and shut-in stage of well operation. In this model, fluid flow in a straight, non-cased two-dimensional well embedded in the two-dimensional formation was considered. The modeling parameters can be found in Table 2. The model domain size of 2500 m in the axial direction and 50 m in the radial direction was chosen to reflect the reservoir depth and to ensure that the lateral outer boundary represents far-field conditions which were not affected by thermal perturbations from well operations. The FE mesh was discretized with 150 layers in the axial direction (\( \Delta z = 16.7 \) m). In the radial direction, the mesh was refined near the well (\( \Delta r_{\text{min}} = 10^{-3} \) m) and coarsened at a larger lateral distance (\( \Delta r_{\text{max}} = 4 \) m). The final mesh size was determined by performing a sensitivity analysis yielding asymptotic smaller variations for the calculated temperatures (maximum temperature variations of less than \( 10^{-2} \) °C). The procedure mentioned above for determining the model domain, mesh sizes, etc., has been applied analogously to each of the models in this work.

The total simulation time was 150 days with 10 days being the cooling (injection) period followed by the shut-in period. The numerically predicted temperatures of borehole fluid during shut-in were used to estimate the SFT according to Eq. 1. The rate of heat transfer during the shut-in period was controlled by the magnitude of the heat transfer coefficient in the model. To investigate the impact of free convection on the
temperature recovery during shut-in, we considered different values of $h_\text{free}$: 0, $h_c$, $9h_c$, $\infty$. According to Eq. (16), the heat transfer coefficients then became: (1) $h = h_c$; (2) $h = 2h_c$; (3) $h = 10h_c$; (4) $h = \infty$. Case (4) corresponds to the condition where the fluid acts as a perfect conductor and thermal resistance in the well does not exist.

**High-temperature environment simulation**

In this section, we focus on the simulation of temperature logs in a high-temperature environment. For this purpose, we have assumed the SFT to be in a temperature range from 5 °C (surface) to 500 °C (bottom-hole). Two different SFT profiles were analyzed. The profile was either linear-shaped which could be linked to a geothermal system controlled by pure heat conduction, or S-shaped representing commonly observed heat convection zones (Fig. 2). The wellbore layout included the drill pipe, annulus and several casings (Table 3). The above-described SFT profiles and wellbore layout were used in each of the following simulation cases.

**Continuous borehole cooling**

The simulations assumed that cold water (7 °C) was injected for 10 days both into the drill pipe and into the annulus at a flow rate of 15 L/s and 45 L/s, respectively (first period). In the second period (thermal recovery), injection into the drill pipe stopped while annulus injection continued but the flow rate was reduced to $Q$ ($Q$ ranged between 0 and 5 L/s). The borehole was under the full shut-in condition when $Q$ was 0 L/s; otherwise, it was under partial shut-in condition. Temperatures of the fluid inside the drill pipe at different warm-up times were measured and then used to estimate SFT by applying the HM.

**Fluid loss**

The impact of fluid loss on the temperature response in a borehole is analyzed by generating a series of dynamic temperature logs based on forward simulations where different fluid loss amounts under different flow rates in the borehole were assumed. These
temperature logs were used as samples for the analysis of the temperature response to the fluid loss in the borehole.

Again cold water (7 °C) was injected through the drill pipe and the annulus separately, and the temperature logs were only ‘recorded’ in the drill pipe. For simplicity, the total amount of fluid being injected was distributed such that the flow velocities in the string and the annulus were equal. The fluid loss occurred at 3.35 km depth from the annulus through a hydraulic connection to the formation. The total amount of injected fluid was varied from 5 to 50 L/s. The percentage of fluid loss from the annulus was varied between 0 and 100%.

**Results and discussion**

**Estimating SFT using shut-in temperature logs**

The evolutions of BHT with respect to time considering four different heat transfer rates are given in Fig. 3a. It is shown that the recovery of BHT is influenced by
the heat transfer rate in the borehole during the early stage of shut-in. The higher the heat transfer rate is, the faster the temperature builds up. A maximum difference of 30 °C between the predicted BHTs is found. However, the four temperature curves have approximately the same build-up rate after 20 days. Furthermore, the sensitivity of temperature build-up on the heat transfer rate decreases when the heat transfer rate reaches $10h_c$. Figure 3b shows the plots of the BHT against the Horner dimensionless time. For each curve, two different BHT data sets are used to estimate the SFT. One contains the early shut-in-time temperature data measured within 1 day ($t_s = 12, 18, 24$ h); another one contains long-term shut-in measurements of several days ($t_s = 2, 3, 4$ days). The regression lines for the early and the long-term shut-in BHT measurements are plotted in Fig. 4a, b, respectively. Figure 4c displays the comparison between the intercepts of these regression lines (SFT estimates) and the true SFT value. In all cases, the SFT is underestimated with a large error when early shut-in-time temperature data are used. The underestimation errors range from $-61.9$ to $-31.3$ °C depending on the rate of heat transfer rate assumed in the model. On the other hand, the accuracy for SFT estimation is improved when using long-term shut-in temperature data, and again, the influence of the heat transfer rate on SFT estimation is observed. The SFT tends to be overestimated under low heat transfer rates ($h = h_c, 2h_c$) and underestimated under higher heat transfer rates ($h = 10h_c, \infty$).
As shown earlier, both the heat transfer rate in the borehole and the measurement time have an impact on the final result of the estimated SFT. In the following SFT calculations, long-term shut-in temperature data measured after 1 day, 2 days and 3 days since the start of the second period were used. The heat transfer coefficient $h$ for the full shut-in conditions was then calibrated by trial and error until an accurate SFT estimation was achieved (see Fig. 5, shut-in case). The calibrated $h$ was examined to be $1.4h_c$ (the SFT estimation error at the bottom-hole was 0.15 °C for the linear SFT profile scenario, and 0.24 °C for the S-shaped SFT profile scenario) and it was used to account for the heat transfer rate within the drill pipe in the second period. In the annulus, forced convection heat transfer dominates the heat transfer process. The SFT was estimated assuming different annulus flow rates and the estimation error at bottom-hole was calculated (Fig. 5). As expected, the SFT was underestimated when temperature measurements under cooling conditions were used in all cases. This is because with continuous cold injection in the annulus during the second period, the temperature was only partially recovered in the borehole compared to the shut-in condition. The higher the flow rate in the annulus was, the less the heat would recover and the larger the resulting underestimation error.

![Figure 4](image-url)

**Fig. 4** The HM plots (lines) using BHT measurements (markers) at **a** early shut-in time ($t_s = 12, 18$ and $24$ h) and **b** long-term shut-in ($t_s = 2, 3, 4$ days) for each of the four different heat transfer coefficients ($h$) considered. **c** Comparison of the results of SFT estimation with the true SFT value: the black bars are the four SFT estimates using early shut-in time BHT data; the dark grey bars represent the four SFT estimates using long-term shut-in BHT data; the solid line stands for the referencing value which is the true SFT (257 °C).
in the SFT (Fig. 5c, d). For small values of flow rate in the annulus up to 0.7 L/s (corresponding fluid velocity of 0.05 m/s at the bottom-hole), the maximum estimation error at the bottom-hole was around 74 °C (percentage error 14.8%) when the linear SFT profile was assumed and 24 °C (percentage error 4.8%) for the S-shaped SFT profile. The reason for the smaller estimation error for the S-shaped profile is the higher SFT value along most parts of the well. Therefore, the fluid is less cooled, resulting in earlier thermal recovery. However, it is noticed that the maximum SFT estimation error along the well depth could be in some cases much greater than the error at the borehole bottom (Fig. 5b, maximum underestimation error of 143 °C was found at 1800 m depth for the flow rate of 0.5 L/s in the annulus).

**Characterization of the fluid loss in the well**

Herein, we present exemplary simulated temperature logs under flow rates of 5 L/s and 50 L/s for an S-shaped SFT profile (Fig. 6). The results for the linear SFT profile were omitted since it was observed that the shape of the SFT profile had a negligible influence on the temperature response to fluid loss. An abrupt increase in the vertical temperature gradient below the loss zone at 3.35 km depth is detected in each temperature log. It is also noticed that the relationship between the increase of the temperature gradient and the percentage of fluid loss is not monotonic. On the one hand, when the percentage of fluid loss is below 95%, a steeper temperature
gradient indicates a higher amount of fluid loss in the borehole. Such behavior can be explained by the fact that with more fluid being lost from the annulus, the fluid remaining in the borehole has more residence time to gain heat from the hotter surroundings and thereby the fluid temperature tends to increase. On the other hand, the increase in the temperature gradient drops when the fluid is almost completely lost. This is due to the fact that very high fluid losses cause very low remaining flow rates. As a result, the heat transfer rate from the formation to the annulus fluid is also strongly impaired. The reduced heat flux results in lower fluid temperatures both in the annulus and drill pipe.

We performed further analyses by calculating the increase of the vertical temperature gradient due to the presence of fluid loss for each of the generated temperature logs. This increase was quantified by computing the ratio of the slope of the temperature profile above the loss zone to the slope below the loss zone. Since the borehole temperature was considered to approach steady-state after 10 days, the temperature slope could be approximated using a linear gradient. The relationship between the gradient ratio and the percentage of fluid loss under different flow rates is illustrated in Fig. 7. The non-monotonic relationship between the gradient ratio and the fluid loss (with maximum temperature gradient ratios occurring when the fluid loss exceeds 95%), which has already been discussed earlier, is observed for each flow rate under consideration. Moreover, the dependence of the gradient ratio on the flow rate seems to be more complex. The gradient ratio tends to be independent of the flow rate if the percentage of fluid loss is low, e.g., < 30%. For fluid losses > 30%, smaller temperature gradient ratios are observed for lower flow rates. However, for flow rates greater than 20 L/s (flow velocity > 0.5 m/s),
the gradient ratio is almost independent to the flow rate except when the fluid loss is greater than 90%.

**Conclusion**

The assessment of geothermal reservoirs relies on the information supplied by logging tools, with temperature logs among the most important ones. The in-house numerical tool developed to simulate the thermal response of the wellbore and the formation during fluid circulation and shut-in conditions is intended to fill the absence of a quantitative interpretation of temperature logs and the associated uncertainties. It accounts especially for the heat transfer process from the formation towards the specific location of the measurement tools including the drill pipe, annulus or open borehole. Particular care is given to the correct treatment of the transient heat transfer through the multiple interfaces (casing–annulus–drill pipe–drill fluid) in such a complex thermal system. The quality of the simulation tool was demonstrated by comparison with borehole temperatures from analytical solutions. In this study, the simulator was applied to generate synthetic shut-in and dynamic temperature logs.

The temperature logs were interpreted for two purposes: SFT estimation and characterization of loss zones. The major findings and the underlying messages conveyed in this study are as follows:

1. The shut-in temperature depends significantly on the magnitude of free convection, which enhances the heat transfer rate. In this study, a maximum difference of 30 °C in BHT predictions between the two extrema scenarios of free convection is found. In this regard, a careful parameterization of the heat transfer rate is especially important in the early transient stage of shut-in heat recovery.
2. The Horner-plot method may strongly underestimate the SFT if early shut-in (within 24 h) temperature measurement data are used. However, it provides high accuracy...
SFT estimates (percentage error < 3%) when using long-term shut-in (2 days up to 4 days) temperature measurement data.

3. Using temperature logs obtained under borehole cooling conditions can become inauspicious for the Horner-plot interpretation method even at small cooling flow rates. This can yield significant errors (24 °C and 74 °C at a flow rate of 0.7 L/s for a linear- and S-shaped SFT, respectively) in the bottom-hole SFT estimation.

4. In the presence of fluid loss, the local temperature gradient change is affected by the flow rate, the percentage of fluid loss as well as the overall rate of the lateral heat transfer from the formation to the borehole fluid. It was found that for fluid losses less than 30%, or under relatively high flow rates (>20 L/s), the gradient change can be independent on the flow rates.

Under the specific conditions of high-temperature boreholes the temperature logging data represent a complex response to the wellbore layout, the flow conditions, the heat transfer mechanism, etc. Under these constraints, a simple interpretation of temperature logs can be strongly misleading and more sophisticated techniques accounting for key factors by numerical simulation are required. Herein, the impacts of these factors were investigated by individual sensitivity analysis. However, in real geothermal applications, these impacts may overlap. Therefore, simulations in this context need to be joined by inverse procedures. In this way, the present contribution represents an important step towards a more sophisticated interpretation of real project data. It requires accounting, in a detailed manner, for the geometrical setting, on the history of injection, drilling, logging (even the time lapse of logging start to logging end) and on the appraisal of measurement errors. Work is now underway to interpret dynamic temperature logs using inverse modeling techniques.

List of symbols

Roman letters

T: temperature (Θ); cp: specific heat capacity (L² T⁻² Θ⁻¹); t: time (T); r: radius (L); v: velocity (L T⁻¹); z: axial coordinate (L); i,j: simulation region number; H: depth (L); m: mass flow rate (M T⁻¹); A: cross-section area (L²); q: heat flux (M T⁻³); Ts: shut-in temperature (Θ); Ts: static formation temperature (Θ); t̅: shut-in time (T); τ: circulation time (T); h: heat transfer coefficient (M T⁻³ Θ⁻¹); Nu: Nusselt number (1); Pr: Prandt number (1); d: diameter (L); L: length (L); ΔT: temperature difference (Θ); Θ: temperature gradient (Θ L⁻¹); Dc: thermal diffusivity (L² T⁻¹); C: constant; SFT: static formation temperature; BHT: bottom-hole temperature; HM: Horner-plot method.

Greek letters

ρ: density (M L⁻³); λ: thermal conductivity (M L T⁻³ Θ⁻¹); Γ: interfacial region; μ: dynamic viscosity (M L⁻¹ T⁻¹); γ: weighting coefficient for linear interpolation; g: the acceleration of gravity (L T⁻²); α: thermal expansion coefficient (Θ⁻¹); ν: kinematic viscosity (L² T⁻¹).

Subscripts

f: fluid; inj: injection; r: radial direction; z: axial direction; wb: wellbore; c: conduction; free: free convection; cr: critical; abs: absolute.

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Authors’ contributions
JW performed the numerical modeling, analysis of the results and wrote the manuscript. FN supervised and provided support in the design of the study. MG provided the numerical simulation tool applied in this study. TK supervised the research and finalization of the manuscript. All authors read and approved the final manuscript.

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Competing interests
The authors declare that they have no competing interests.

Appendix
Appendix A. Validation of the Ramey’s heat transmission model
Most of the literature on wellbore heat transmission is based on the classical work of Ramey (Ramey 1962, 1964). A simple physical model that describes the wellbore heat transmission consists of fluid flow in a straight, non-cased, one-dimensional well which is embedded in the two-dimensional formation. Ramey derived an analytical solution for the transient temperature distribution in injection and production wells based on simplified heat balances. However, it was found that Ramey’s solution is normally valid for long times but is significantly inaccurate for early-stage transient periods. A number of studies have attempted to adjust Ramey’s solution and derive more efficient and stable approximations to small, medium, and large-time solutions by giving specific expressions in terms of the so-called dimensionless time function which represents the transient heat transfer from wellbore to the formation (Kutasov 1987, 2003; Wu and Pruess 1988; Hagoort 2004; Kutun et al. 2014, 2015). In this work, we adopted the simplified expression for dimensionless time function given by Kutun et al. (2015), which is based on the best curve fit of Ramey’s dimensionless time function data.

The injection and production cases were modeled by considering three different scenarios: (i) water being injected at the same temperature as the surface temperature; (ii) water being injected at a higher temperature than the surface temperature; (iii) water being extracted from the reservoir. The model set up and geometry and thermal properties data used in the simulations were the same as defined in “Shut-in temperature logs simulation”, except that the well with 0.15 m radius is simplified as a one-dimensional structure.

Figure 8 presents a comparison of temperatures obtained from analytical solutions given by Ramey (Ramey 1962) and our numerical models. Maximum temperature differences (errors) for the three different simulations on day 1, day 5 and day 10, respectively. Case (i): $|\Delta T|_{\text{max}} \leq 1.9 \degree C$, case (ii): $|\Delta T|_{\text{max}} \leq 0.21 \degree C$, and case (iii): $|\Delta T|_{\text{max}} \leq 1.9 \degree C$. 
Appendix B. Validation of the counterflow heat exchange model

The counterflow heat exchange model is essentially the physical model for mud circulation under the drilling process in a wellbore. During circulation, the drilling mud flows downwards (axial direction) in the drill pipe. The heat exchange process of the system involves two mechanisms: convective heat transport and heat transfer of the drilling mud with the pipe wall (forced convection heat transfer). At the bottom, fluid exited through the drill bit into the annulus. The temperatures at the outlet of the drill pipe and the inlet of the annulus are considered to be the same. The fluid in the annulus moves upwards to the surface. The annulus fluid temperature is controlled by the rate of convective heat transport and forced convection heat transfer at two fluid–solid interfaces: annulus fluid/outer drill pipe wall, annulus fluid/wellbore wall.

The model size was 4600 m in the axial direction and 50 m in the radial direction. The mesh was discretized in 15 m steps in the axial direction, mesh sizes in the radial direction ranged between $10^{-3}$ and 6.5 m. The geometric parameters of the wellbore and thermal properties data used in the modeling are given in Table 4. The analytical solution for the fluid temperature distribution inside the drill pipe and the annulus given by Bobok and Szarka (2012) was used for the numerical validation of the mud circulation model. The comparison of the analytical solution and the simulated solution of the drill pipe fluid and annulus temperature is shown in Fig. 9. Maximum estimation differences for the temperature of drill pipe fluid and annulus fluid were calculated, respectively: 0.72 °C, 1.06 °C after 4 days’ circulation; 0.32 °C, 0.51 °C after 10 days’ circulation; 0.08 °C, 0.17 °C after 20 days’ circulation (Table 4).
Table 4 Geometric parameters and material properties used in the simulation of the counterflow heat exchange model

| Property                                      | Unit     | Value  |
|-----------------------------------------------|----------|--------|
| Formation temperature at the surface         | °C       | 7      |
| The geothermal gradient                      | °C/m     | 0.1    |
| Casing thermal conductivity                  | W/(m °C) | 50     |
| Cement thermal conductivity                  | W/(m °C) | 1.2    |
| Formation rock density                       | kg/m³    | 3000   |
| Formation thermal conductivity               | W/(m °C) | 1.5    |
| Formation specific heat capacity             | J/(kg °C)| 840    |
| Well depth                                   | m        | 4600   |
| Inside radius of the drill pipe              | m        | 0.0352 |
| The outside radius of the drill pipe         | m        | 0.0445 |
| Inside radius of the casing                  | m        | 0.0797 |
| The outside radius of the casing             | m        | 0.089  |
| The radius of the wellbore/formation interface | m    | 0.1    |
| Water production rate                        | kg/s     | 15     |
| Water specific heat capacity                 | J/(kg °C)| 4194   |
| Water density                                | kg/m³    | 1000   |
| Water viscosity                              | Pa s     | 1e−3   |
| Water thermal conductivity                   | W/(m °C) | 0.6    |

Fig. 9 Comparison of analytical solution and simulated solution for the counterflow heat exchange model. Black color represents the temperature of the fluid inside the drill pipe, red color represents the temperature of annulus fluid. Solutions were calculated and compared at three different circulation time: 5 days, 10 days, 20 days. The analytical solution was plotted in lines: solid lines (5 days), dash-dot lines (10 days), dot lines (20 days). The simulated solution was marked in symbols: circles (5 days), squares (10 days), crosses (20 days).
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