Are Nearby Neighbors Relatives? Testing Deep Music Embeddings

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Deep neural networks have frequently been used to directly learn representations useful for a given task from raw input data. In terms of overall performance metrics, machine learning solutions employing deep representations frequently have been reported to greatly outperform those using hand-crafted feature representations. At the same time, they may pick up on aspects that are predominant in the data, yet not actually meaningful or interpretable. In this paper, we therefore propose a systematic way to test the trustworthiness of deep music representations, considering musical semantics. The underlying assumption is that in case a deep representation is to be trusted, distance consistency between known related points should be maintained both in the input audio space and corresponding latent deep space. We generate known related points through semantically meaningful transformations, both considering imperceptible and graver transformations. Then, we examine within- and between-space distance consistencies, both considering audio space and latent embedded space, the latter either being a result of a conventional feature extractor or a deep encoder. We illustrate how our method, as a complement to task-specific performance, provides interpretable insight into what a network may have captured from training data signals.

Keywords: music information retrieval, neural network, representation learning, evaluation, MFCC

1. INTRODUCTION

Music audio is a complex signal. Frequencies in the signal usually belong to multiple pitches, which are organized harmonically and rhythmically, and often originate from multiple acoustic sources in the presence of noise. When solving tasks in the Music Information Retrieval (MIR) field, within this noisy signal, the optimal subset of information needs to be found that leads to quantifiable and musical descriptors. Commonly, this process is handled by pipelines exploiting a wide range of signal processing and machine learning algorithms. Beyond the use of hand-crafted music representations, which are informed by human domain knowledge, as an alternative, deep music representations have emerged, that are trained by employing deep neural networks (DNNs) and massive amounts of training data observations. Such deep representations are usually reported to outperform hand-crafted representations (e.g., [1–4]).

At the same time, the performance of MIR systems may be vulnerable to subtle input manipulation. The addition of small noise may lead to unexpected random behavior, regardless of whether traditional or deep models are used [5–8]. In a similar line of thought, in the broader deep learning (DL) community, increasing attention is given to adversarial examples that are barely differentiable from original samples, but greatly impact a network’s performance [8, 9].
So far, the sensitivity of representations with respect to subtle input changes has mostly been tested in relation to dedicated machine learning tasks (e.g., object recognition, music genre classification), and examined by investigating whether these input changes cause performance drops. When purely considering the questions whether relevant input signal information can automatically be encoded into a representation, and to what extent the representation can be deemed “reliable,” in principle, the learned representation should be general and useful to different types of tasks. Therefore, in this work, we will not focus on performance obtained by using a learned representation for certain machine learning tasks, but rather on a systematic way to verify assumptions on distance relationships between several representation spaces: the audio space and the learned space.

Inspired by Sturm [5], we will also investigate the effect of musical and acoustic transformations of audio input signals, in combination with an arbitrary encoder of the input signal, which either may be a conventional feature extractor or deep learning-based encoder. In doing this, we have the following major assumptions:

(i) If a small, humanly imperceptible transformation is introduced, the distance between the original, and transformed signal should be very small, both in the audio and encoded space. This is illustrated in Figure 1

(ii) However, if a more grave transformation is introduced, the distance between the original and transformed signal should be larger, both in the audio and encoded space.

(iii) The degree of how these assumptions hold will differ for the tasks and the datasets on which the encoder is trained.

To examine the above assumptions, we seek to answer the following research questions:

RQ 1. Do assumption (i) and (ii) hold for conventional and deep learning-based encoders?
RQ 2. Does assumption (iii) hold for music-related tasks and corresponding datasets, especially when deep learning is applied?

By answering the above questions, ultimately we seek to test if considered music-related encoders hold a desirable consistency, such that the distances between audio space and the latent space are monotonically related.

With this work, we intend to offer directions toward a complementary evaluation method for deep machine learning pipelines, that focuses on space diagnosis rather than the troubleshooting of pipeline output. Our intention is that this will provide the researcher with additional insight into the reliability and potential semantic sensitivities of deep learned spaces.

In the remainder of this paper, we first describe our approaches including the details on the learning setup (section 2) and the methodology to assess distance consistency (section 3), followed by the experimental setup (section 4). Further, we report the result from our experiments (section 5). Afterwards we discuss the results and conclude this work (section 6).

## 2. LEARNING

To diagnose a deep music representation space, such a space should first exist. For this, one needs to find a learnable deep encoder $f : \mathbb{R}^{t \times b} \rightarrow \mathbb{R}^d$ that transforms the input audio representation $x \in \mathbb{R}^{t \times b}$ to a latent vector $z \in \mathbb{R}^d$, while taking into account the desired output for a given learning task. The learning of $f$ can be done by adjusting the parameterization θf to optimize the objective function, which should be defined in accordance to a given task.

### 2.1. Tasks

In our work, we consider representations learned for four different tasks: autoencoder (AE), music auto-tagging (AT), predominant instrument recognition (IR), and finally singing voice separation (VS). By doing this, we take a broad range of problems into account that are particularly common in the MIR field. AE is a representative task for unsupervised learning using DNNs, and AT is a popular supervised learning task in the MIR field [3, 10–14]. AT is a multi-label classification problem, in which individual labels are not always mutually exclusive and often highly inter-correlated. As such, it can be seen as a more challenging problem than IR, which is a single-label classification problem. Furthermore, IR labels involve instruments, which can be seen as more objective and taxonomically stable labels than

![FIGURE 1](image-url) Simplified example illustrating distance assumption within a space. Circles without a cross indicate music clips. Yellow circles with crosses refer to hardly perceptible transformations of the yellow original clip. The top-right transformation, marked with a red outer circle, actually is closer to another original clip (green) than to its own original (yellow), which violates the assumption it should be closest to its original, and hence may be seen as an error-inducing transformation under a nearest-neighbor scheme.
e.g., genres or moods. Finally, VS is a task that can be formulated as a regression problem, that learns a mask to segregate a certain region of interest out of a given signal mixture.

2.1. Autoencoder
The objective of an autoencoder is to find a set of encoder $f$ and decoder $g$ functions such that the input audio $x$ is encoded into a fixed-length vector and reconstructed as follows:

$$\hat{x} = g(f(x))$$

(1)

Here, the $\hat{x} = g(f(x))$ is the output of a cascading pipeline of a decoder $g : \mathbb{R}^d \rightarrow \mathbb{R}^{t \times b}$ parameterized by $\Theta_g$, followed by an encoder $f$. To obtain a desired model, a reconstruction error is typically considered as its loss function:

$$J^{AE} = \sum_{i=1}^{|X|} \|x^i - \hat{x}^i\|_2$$

(2)

where $X_r$ is the given set of training samples for the autoencoder task.

2.1.2. Music Auto-Tagging
Unlike the autoencoder, a DNN model architecture for either multi-label or multi-class classification has architectural block $h$ to infer the posterior distribution of classes from the encoding by $f$:

$$\hat{y} = \sigma(h(f(x)))$$

(3)

Since we consider a single fully-connected layer as $h$ in this study, $h : \mathbb{R}^d \rightarrow \mathbb{R}^K$ is the prediction layer parameterized by $\Theta_h$, which transforms the deep representation $z^i$ into the logit per class, which is finally mapped into $p(k|x^i)$ by the sigmoid function $\sigma$.

The typical approach to music auto-tagging using DNNs is to consider the problem as a multi-label classification problem, for which the objective is to minimize the binary cross-entropy of each music tag $k \in \{1, 2, ..., K\}$, which is expressed as follows:

$$J^{AT} = -\sum_{i=1}^{|X|} \sum_{k=1}^{K} y^i_k \log (\hat{y}^i_k) + (1 - y^i_k) \log (1 - \hat{y}^i_k)$$

(4)

where $y^i_k$ is the binary label that indicates whether the tag $k$ is related to the input audio signal $x^i$. Similarly, $\hat{y}^i_k$ indicates the inferred probability of $x^i$ and tag $k$. The optimal functions $f$ and $h$ are found by adjusting $\Theta_f$ and $\Theta_h$ such that (4) is minimized.

2.1.3. Predominant Musical Instrument Recognition
The learning of the IR task can be formulated as a single-label, multi-class classification, which allows one to use a model architecture similar to the aforementioned one, except the terminal non-linearity:

$$\hat{y} = \text{softmax}(h(f(x)))$$

(5)

Here, the softmax function $\text{softmax}(o) = \frac{e^o}{\sum_{i=1}^{c}e^i}$, where $o \in \mathbb{R}^T$ is the output of $h$, substitutes the sigmoid function in (3) to output the categorical distribution over the class.

To maximize the classification accuracy, one of the popular loss function especially in the context of neural network learning is categorical cross-entropy, given as follows:

$$J^{IR} = -\sum_{i=1}^{N} \sum_{t=1}^{T} y^i_t \log (\hat{y}^i_t)$$

(6)

where $t \in \{1, 2, ..., T\}$ is a instrument class and thus, $\hat{y}^i_t$ is the binary label of instance $x^i$ to the class $t$ and $y^i_t$ indicates the inferred probability of $x^i$ and instrument $t$, respectively.

2.1.4. Singing Voice Separation
There are multiple ways to set up an objective function for the source separation task. It can be achieved by simply applying (2) between the output of the network $\hat{x} = g(f(x))$ and the desired isolated signal $y^i \in \mathbb{R}^{t \times b}$ such that the model can infer direct isolated sound. In this case, the objective function is similar to (2), except that the target is substituted from the input signal $x$ to the isolated signal $y$. On the other hand, as introduced in Jansson et al. [15], one can learn a model predicting the mask that segments the target component from the mixture as follows:

$$\hat{x} = \sigma(g(f(x))) \odot x$$

(7)

where $\hat{x}$ is the estimated isolated signal and $x \in \mathbb{R}^{t \times b}$ is the representation of the original input mixture, and $\odot$ refers to the element-wise multiplication. $\sigma(g(f(x))) \in \mathbb{R}^{t \times b}$ is the mask inferred by $g$ and $f$ of which the elements are bounded in the range $[0, 1]$ by the sigmoid function $\sigma$, such that they can be used for the separation of the target source. As introduced in Jansson et al. [15], we applied the skip connections.

For the optimization of the encoder parameters $\Theta_f$ and the decoder parameters $\Theta_g$, [15] suggests to use the L1 loss as follows:

$$J^{VS} = \sum_{i=1}^{|X|} \|s^i - \hat{s}^i\|_1$$

(8)

where $s^i$ is the low-level representation of the isolated signal, which serves as the regression target. Note, that both input $x^i$ and estimated target source $\hat{s}$ are magnitude spectra, so we use the original phase of input $x^i$ to reconstruct a time-domain signal.

2.2. Network Architectures
The architecture of a DNN determines the overall structure of the network, which defines the details of the desired patterns to be captured by the learning process [16]. In other words, it reflects the way in which a network should interpret a given input data representation. In this work, we use a VGG-like architecture, one of the most popular and general architectures frequently employed in the MIR field.

The VGG-like architecture is a Convolutional Neural Network (CNN) architecture introduced by [17, 18], which employs tiny rectangular filters. Successes of VGG-like architectures have not only been reported for computer vision tasks, but also in various MIR fields [3, 8]. The detailed architecture design used in our work can be found in the Table 1 and Figure 2.
will assess their reliability by examining the distance consistency. A map from a dataset and excerpts belong to, we obtain the transformed points \( x_t = \tau(x) \) and \( z_t = f(z_t) \), and then we calculate the error function \( \delta \) of each transformed sample as follows:

\[
\delta(p, \mathcal{P}, \tau, d) = \begin{cases} 
0, & \text{if } d(p, p') < d(p, p'), \forall p' \in \mathcal{P} \setminus p \\
1 & \text{otherwise} 
\end{cases}
\]

Where \( p \in \mathcal{P} \) can be either audio samples \( x \in \mathcal{X} \) or latent points \( z \in \mathcal{Z} \), according to the target space to be measured. Finally, \( d \) is a distance function between two objects.

As \( \delta \) indicates how the space is unreliable at the exemplar-level, the within-space consistency can be defined as the complement of \( \delta \):

\[
C^W = 1 - E_{p \in \mathcal{P}}[\delta(p, \mathcal{P}, \tau, d)]
\]

3.1.2. Between-Space Consistency

To measure consistency between the associated spaces, one can measure how they are correlated. The distances between a transformed point \( p_t \) and its original sample \( p \) will be used as characteristic information to make comparisons between spaces. As mentioned above, we consider two specific spaces: the audio input space \( \mathcal{A} \) and the embedding space \( \mathcal{L} \). Consequently, we can calculate the correlation of distances for the points belonging to each subset of spaces as follows:

\[
C^B = \rho(d^{A}_{\tau}, d^{\mathcal{L}}_{\tau})
\]

where \( \rho \) is Spearman’s rank correlation, and \( d^{A}_{\tau} \) and \( d^{\mathcal{L}}_{\tau} \) refers to the distance array \( d(x_t, x') \) and \( d(z_t, z'), \forall x' \in \mathcal{X}^{\text{ts}} \setminus x \), respectively.

On the other hand, one can also simply measure the agreement between distances, which is given by:

\[
C_{\text{ace}}^B = \text{accuracy}(\delta^{d, \tau}_{\mathcal{A}}, \delta^{d, \tau}_{\mathcal{L}})
\]

where \( \text{accuracy} \) denotes the binary accuracy function [23], and \( \delta^{d, \tau}_{\mathcal{A}} \) and \( \delta^{d, \tau}_{\mathcal{L}} \) denote \( \delta(x, \mathcal{X}, \tau, d) \) and \( \delta(z, \mathcal{Z}, \tau, d) \), respectively.

3.2. Distance Measures

The main assessment of this work is based on distance comparisons between original clip fragments and their transformations, both in audio and embedded space. To our best knowledge, not many general ways are developed to calculate perturbation from literature, we intentionally avoid using the term, since we also study more grave ranges of deformations which are not usually studied.
the distance between raw audio representations of music signals directly. Therefore, we choose to calculate the distance between audio samples using time-frequency representations as the potential proxy of perceptual distance between the music signals. More specifically, we use Mel Frequency Cepstral Coefficients (MFCCs) with 25 coefficients, dropping the first coefficient when the actual distance is calculated. Eventually, we employ two distance measures on the audio domain:

- Dynamic Time Warping (DTW) is a well-known dynamic programming method for calculating similarities between time series. For our experiments, we use the FastDTW implementation [24].
- Similarity Matrix Profile (SiMPle) [25] measures the similarity between two given music recordings using a similarity join [25]. We take the median of the profile array as the overall distance between two audio signals.

For deep embedding space, since any deep representation of input \( x \) is encoded as a fixed-length vector \( z \) in our models, we adopted two general distance measures for vectors: Euclidean distance and cosine distance.

### 3.3. Transformations

In this subsection, we describe the details on the transformations we employed in our experiment. In all cases, we will consider a range from very small, humanly imperceptible transformations, up to transformations within the same category, that should be large enough to become humanly noticeable. While it is not trivial to set an upper bound for the transformation magnitudes, at which a transformed sample may be recognized as a “different” song from the original, we introduce a reasonable range of magnitudes, such that we can investigate the overall robustness of our target encoders as transformations will become more grave. The selected range per each transformation is illustrated in Figure 3.

- **Noise**: As a randomized transformation, we applied both pink noise (PN) and environmental noise (EN) transformations.
More specifically, for EN, we used noise recorded in a bar, as collected from freesound\textsuperscript{2}. The test range of the magnitude, expressed in terms of Signal to Noise Ratio, spans from –15 to 30 dB, with denser sampling for high Signal to Noise Ratios (which are situations in which transformed signals should be very close to the original signal) \cite{26}. This strategy also is adopted for the rest of the transformations.

- Tempo Shift: We applied a tempo shift (TS), transforming a signal to a new tempo, ranging from 30% to 150% of the original tempo. Therefore, we both slow down and speed up the signal. Close to the original tempo, we employed a step size of 2\%, as a –2 and 2\% tempo change has been considered as an irrelevant slowdown or speedup in previous work \cite{5}. We employed an implementation\textsuperscript{3} using a phase vocoder and resampling algorithm.

- Pitch Shift: We also employed a pitch shift (PS), changing the pitch of a signal, making it lower or higher. Close to the original pitch, we consider transformation steps of ±25 cents, which is 50\% smaller than the error bound considered in the MIREX challenge of multiple fundamental frequency

\textsuperscript{2}https://freesound.org

\textsuperscript{3}https://breakfastquay.com/rubberband/
estimation & tracking [27]. Beyond a difference of 1 semitone with respect to the original, whole tone interval steps were considered.

- Compression: For compression (MP), we simply compress the original audio sample using an MP3 encoder, taking all kb/s compression rates as provided by the FFmpeg software [28].

For the rest of the paper, for brevity, we use OG as the acronym of the original samples.

4. EXPERIMENT

4.1. Audio Pre-processing

For the input time-frequency representation to the DNNs, we use the dB-scale magnitude STFT matrix. For the calculation, the audio was resampled at 22,050 kHz. The window and overlap size are 1,024 and 256 respectively. It leads to the dimensionality of the frequency axis to be \( b = 513 \), only taking positive frequencies into account. The standardization over the frequency axis is applied by taking the mean and the standard deviation of all magnitude spectra in the training set.

Also, we use the short excerpts of the original input audio track with \( t = 128 \), which yields \( \sim 2 \) s per excerpt in the setup we used. Each batch of excerpts is randomly cropped from 24 randomly chosen music clips before being served to the training loop.

When applying the transformations, it turned out that some of the libraries we used did not only apply the transformation, but also changed the loudness of the transformed signal. To mitigate this, and only consider the actual transformation of interest, we applied a loudness normalization based on the EBU-R 128 loudness measure [29]. More specifically, we calculated the mean loudness of the original sample, and then ensured that transformed audio samples would have equal mean loudness to their original.

4.2. Baseline

Beyond deep encoders, we also consider a conventional feature extractor: MFCCs, as also used in [10]. The MFCC extractor can also be seen as an encoder, that projects raw audio measurements into a latent embedding space, where the projection was hand-crafted by humans to be perceptually meaningful.

We first calculate the first- and second-order time derivatives of the given MFCCs and then take the mean and standard deviation over the time axis, for the original and its derivatives. Finally, we concatenate all statistics into one vector. Using the 25 coefficients excluding the first coefficient, we obtain \( z_{\text{MFCC}} \in \mathbb{R}^{144} \) from all the points in \( X^{|\tau} \). For the AT task, we trained a dedicated \( h \) for auto-tagging, with the same objective as Equation 4, while \( f \) is substituted as \( z_{\text{MFCC}} \).

4.3. Dataset

We use a subset of the Million Song Dataset (MSD) [30] both for training and testing of AT and AE task. The number of the training samples \( |X^{|\tau}| \) is 71,512. These are randomly drawn from the original subset of 102,161 samples without replacement. For the test set \( X^{|\tau} \), we used 1,000 excerpts randomly sampled from 1,000 preview clips which are not used at training time. As suggested in Choi et al. [3], we used the top \( K = 50 \) social tags based on their frequency within the dataset.

As for the IR task, we choose to use the training set of the IRMAS dataset [31], which contains 6,705 audio clips of 3 s polyphonic mixtures of music audio, from more than 2,000 songs. The pre-dominant instrument of each short excerpt is labeled. As excerpts may have been clipped from a single song multiple times, we split the dataset into training, validation and test sets at the song level, to avoid unwanted bleeding among splits.

Finally, for VS, we employed the MUSDB18 dataset [32]. This dataset is developed for musical blind source separation tasks, and has been used in public benchmarking challenges [33]. The dataset consists of 150 unique full-length songs, both with mixtures and isolated sources of selected instrument groups: vocals, bass, drums and other. Originally, the dataset is split into a training and test set; we split the training set into a training and validation set (with a 7:3 ratio), to secure validation monitoring capability.

Note that since we use different datasets with respect to the tasks, the measurements we investigate will also depend on the datasets and tasks. However, across tasks, we always use the same encoder architecture, such that comparisons between tasks can still validly be made.

4.4. Performance Measures

As introduced in section 3, we use distance consistency measures as primary evaluation criterion of our work. Next to this, we also measure the performance per employed learning task. For the AE task, the Mean Square Error (MSE) is used as a measure of reconstruction error. For the AT task, we apply a measure derived from the popular Area Under ROC Curve (AUC): more specifically, we apply \( AUC_C \), averaging the AUC measure over clips. As for the IR task, we choose to use accuracy. Finally, for VS, we employed the MUSDB18 dataset [32].

While beyond SDR, this software suite also can calculate 3 more evaluation measures (Image to Spatial distortion Ratio (ISR), Source to Interference Ratio (SIR), Sources to Artifacts Ratios (SAR)), in this study, we choose to only employ SDR: the other metrics consider spatial distortion, while this is irrelevant to our experimental setup, in which we only use mono sources.

5. RESULTS

In the following subsections, we present the major analysis results for task-specific performance, within-space consistency, and finally, between-space consistency. Shared conclusions and discussions following from our observations will be presented in section 6.

5.1. Task-Specific Performance

To analyze task-specific performance, we ran predictions for the original samples in \( X^{|\tau} \), as well as their transformations using all \( \tau \in \mathcal{T} \) with all the magnitudes we selected. The overall results,
grouped by transformation, task and encoder, are illustrated in Figure 4. For most parts, we observe similar degradation patterns within the same transformation type. For instance, in the presence of PN and EN transformations, performance decreases in a characteristic non-linear fashion as more noise is added. The exception seems to be the AE task, which shows somewhat unique trends with a more distinct difference between encoders. In particular, when EN is introduced, performance increases with the severity of the transformation. This is likely to be caused by the fact that the environmental noise that we employed is semantically irrelevant for the other tasks, thus causing a degradation in performance. However, because the AE task just reconstructs the given input audio regardless of the semantic context, and the environmental noise that we use is likely not as complex as music or pink noise, the overall reconstruction gets better.

To better understand the effect of transformations, we fitted a Generalized Additive Model (GAM) on the data, using as predictors the main effects of the task, encoder and transformation, along with their two-factor interactions. Because the relationship between performance and transformation magnitude is very characteristic in each case, we included an additional spline term to smooth the effect of the magnitude for every combination of transformation, task and encoder. In addition, and given the clear heterogeneity of distributions across tasks, we standardized performance scores using the within-task mean and standard deviation scores. Furthermore, MSE scores in the AE task are reversed, so that higher scores imply better performance. The analysis model explains most of the variability ($R^2 = 0.98$).

An Analysis on Variance (ANOVA) using the marginalized effects clearly reveals that the largest effect is due to the encoders.
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5.2. Within-Space Consistency

In terms of within-space consistency, we first examine the mean performance. ± followed by IR (0.539 like cases, AT shows the highest consistency (0.671 consistency (0.741 from the plots that the MFCC encoder has significantly higher cosine distance measures. In general, the trends are similar to model, including the main effect of the transformation and task, Figure 6 with respect to Euclidean distance, this analysis model achieved R^2 with respect to transformations. As transformations have higher magnitude, as expected, the consistency decreases, but at different rates, depending on the transformation. The clear exception is the TS transformation, where both measures, and in particular DTW, are highly robust to the magnitude of the shift. This result implies that the explicit consideration of both measures on the temporal dynamics can be beneficial.

With respect to the within-consistency of the latent space, Figures 7, 8 depicts the results for both the Euclidean and cosine distance measures. In general, the trends are similar to those found in Figure 6. For analysis, we fitted a similar GAM model, including the main effect of the transformation and task, their interaction, and a smoother for the magnitude of each transformation within each task. When modeling consistency with respect to Euclidean distance, this analysis model achieved R^2 = .98. An ANOVA analysis shows very similar effects due to transformation [F(4,1793)=1087, p < 0.0001] and due to tasks [F(4,1793)=1066, p < 0.0001], with a smaller effect of the interaction. In particular, the model confirms the observation from the plots that the MFCC encoder has significantly higher consistency (0.741 ± 0.014) than the others. For the VGG-like cases, AT shows the highest consistency (0.671 ± 0.007), followed by IR (0.539 ± 0.008), VS (0.331 ± 0.007) and lastly by AE (0.17 ± 0.006). As Figure 8 shows, all these differences are statistically significant.

A similar model to analyze consistency with respect to the cosine distance yielded very similar results (R^2 = 0.981). However, the effect of the task [F(4,1794) = 1263, p < 0.0001] was larger than the effect of the transformation [F(4,1794) = 913, p < 0.0001], indicating that the cosine distance is slightly more robust to transformations than the Euclidean distance.

To investigate observed effects more intuitively, we visualize in Figure 9 the original dataset samples and their smallest transformations, which should be hardly perceptible to imperceptible to human ears [5, 8, 27] in a 2-dimensional space, using t-SNE [34].

5.3. Between-Space Consistency

Next, we discuss between-space consistency according to C^B acc and C^B, as discussed in section 3.1.2. As in the previous section, we first provide a visualization of the relationship between transformations and consistency, and then employ the same GAM model to analyze individual effects. The analysis will be presented for all pairs of distance measures and between-space consistency measures, which results in 4 models for C^B acc and another 4 models for C^B. As in the within-space consistency analysis, we set the MFCC and other VGG-like networks from different learning tasks as independent “encoder” f to a latent embedded space.

5.3.1. Accuracy: C^B acc

The between-space consistency, according to the C^B acc criterion, is plotted in the upper plots of Figure 10. Comparing this plot to the within-space consistency plots for A (Figure 6) and L (Figure 8), one trend is striking: when within-space consistency is low and L becomes substantially low, the between-space consistency C^B acc becomes high. This can be interpreted: when grave transformations are applied, the within-space consistencies in both A and L space will converge to 0, and comparing the two spaces, this behavior is consistent.

A first model to analyze the between-space consistency with respect to the SiMPLe and cosine measures (R^2 = 0.96), reveals that the largest effect is that of the task/encoder [F(4,1772) = 440, p < 0.0001], followed by the effect of the transformation [F(4,1772) = 285, p < 0.0001]. The left plot of the first row in Figure 11 confirms that the estimated consistency of the MFCC encoder (0.796 ± 0.015) is significantly higher than that of the VGG-like alternatives, which range between 0.731 and 0.273. In fact, the relative order is the same as observed in the within-space case: MFCC is followed by AT, IR, VS, and finally AE.

We separately analyzed the data with respect to the other three combinations of measures, and found very similar results. The largest effect is due to the task/encoder, followed by the transformation; the effect of the interaction is considerably

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4The smallest transformations are ±25 cents in PS, ±2% in TS, 30 dB in PN and EN, and 192 kb/s in MP.
smaller. As the first rows of Figure 11 show, the same results are observed in all four cases, with statistically significant differences among tasks.

5.3.2. Correlation: $C^B_{\rho}$

The bottom plots in Figure 10 show the results for between-space consistency measured with $C^B_{\rho}$. It can be clearly seen that MFCC
preserves the consistency between spaces much better than VGG-like encoders, and in general, all encoders are quite robust to the magnitude of the perturbations.

Analyzing data again using a GAM model confirms these observations. For instance, when analyzing consistency with respect to the DTW and Euclidean measures ($R^2 = 0.96$), the
largest effect is by far that of the task/encoder \( F(4,1877) = 6549, p < 0.0001 \), with the transformation and interaction effect being two orders of magnitude smaller. This is because of the clear superiority of MFCC, with an estimated consistency of 0.881 ± 0.004, followed by AE (0.209 ± 0.005), IR (0.184 ± 0.003), VS (0.181 ± 0.002), and finally AT (0.08 ± 0.003) (see right plot of the fourth row in 11).

As before, we separately analyzed the data with respect to the other three combinations of measures, and found very similar results. As first two rows of Figure 11 shows, the same qualitative observations can be made in all four cases, with statistically significant differences among tasks. Noticeably, the superiority of MFCC is even clearer when employing the Euclidean distance.

5.4. Sensitivity to Imperceptible Transformations

5.4.1. Task-Specific Performance

In this subsection, we focus more on the special cases of transformations with a magnitude small enough to hardly be perceivable by humans \([5, 8, 27]\) As the first row of Figure 12 shows, performance is degraded even with such small transformations, confirming the findings from \([5]\). In particular, the VS task shows more variability among transformations compared to other tasks. Between transformations, the PS cases show relatively higher degradation.

5.4.2. Within-Space Consistency

The second row of Figure 12 illustrates the within-space consistency on the \( L \) space when considering these smallest transformations. As before, there is no substantial difference between the distance metrics. In general, the MFCC, AT, and IR encoder/tasks are relatively robust on these small transformations, with their median consistencies close to 1. However, encoders trained on the VS and AE tasks show undesirably high sensitivity to these small transformations. In this case, the effect of the PS transformations is even more clear, causing considerable variance for most of the tasks. The exception is AE, which is more uniformly spread in the first place.

5.4.3. Between-Space Consistency

Finally, the between-space consistencies on the minimum transformations are depicted in the last two rows of Figure 12. First, we see no significant differences between pairs of distance measures. When focusing on \( C_B^\text{acc} \), the plots highly resemble those from 5.4.2, which can be expected, because the within-space consistency on \( A \) is \( \sim 1 \) for all these transformations, as illustrated in Figure 6. On the other hand, when focusing on \( C_B^\rho \), The last row of Figure 12 shows that even such small transformations already result in large inconsistencies between spaces when employing neural network representations.

6. DISCUSSION AND CONCLUSION

6.1. Effect of the Encoder

For most of our experiments, the largest differences are found between encoders. As is well-known, the VGG-like deep neural network shows significantly better task-specific performance in comparison to the MFCC encoder. However, when considering distance consistency, MFCC is shown to be the most consistent encoder for all cases, with neural network approaches performing substantially worse in this respect. This suggests that, in case a task requires robustness to potential musical/acoustical
deviations in the audio input space, it may be more preferable to employ MFCCs than neural network encoders.

### 6.2. Effect of the Learning Task

Considering the neural networks, our results show that the choice of learning task is the most important factor affecting consistency. For instance, a VGG-like network trained on the AE task seems to preserve the relative distances among samples (high $C^B_{\text{acc}}$), but individual transformed samples will fall closer to originals that were not the actual original the transformation was applied to (low $C^B_{\text{acc}}$). On the other hand, a task like AT yields high consistency in the neighborhood of corresponding original samples (high $C^B_{\text{acc}}$). This means that a network trained on a low-level task like AE is more consistent than a network trained on a high-level task like AT, because the resulting latent space is less morphed and it more closely resembles the original audio space. In fact, in our results we see that the semantic high-levelness of the task (AT > IR > VS > AE) is positively correlated with $C^B_{\text{acc}}$, while negatively correlated with $C^B_{\text{p}}$.

To further confirm this observation, we also computed the between-space consistency $C^B_{\text{p}}$ only on the set of original samples. The results, in Figure 13, are very similar to those in the last two rows of Figures 11, 12. This suggests that in general, the global distance structure of an embedded latent space with respect to the original samples generalizes over the vicinity of those originals, at least for the transformations that we employed.

Considering that AE is an unsupervised learning task, and its objective is merely to embed an original data point into a low-dimensional latent space by minimizing the reconstruction error, the odds are lower that data points will cluster according to more semantic criteria, as implicitly encoded in supervised learning tasks. For instance, in contrast, the VS task should morph the latent space such that input clips with similar degrees of "vocalness" should fall close together, as indeed is shown in Figure 14. As the task becomes more complex and high-level, such as with AT, this clustering effect will become more multi-faceted and complex, potentially morphing the latent space with respect to the semantic space that is used as the source of supervision.

### 6.3. Effect of the Transformation

Across almost all experimental results, significant differences between transformation categories are observed. On the one hand, this supports the findings from Sturm [5] and Kereliuk et al. [8], which show the vulnerability of MIR systems to small audio transformations. On the other hand, this also implies that different types of transformations have different effects on the latent space, as depicted in Figure 7.

### 6.4. Are Nearby Neighbors Relatives?

As depicted in Figure 7, substantial inconsistencies emerge in $\mathcal{L}$ when compared to $\mathcal{A}$. Clearly, these inconsistencies
FIGURE 12 | Performance, within-space consistency, and between-space consistency on the minimum transformations. The points are individual observations with respect to the transformation types. For PS and TS, we distinguish in the direction of the transformation (+: pitch/tempo up, -: pitch/tempo down). The first row indicates the task-specific performance, and the second row depicts the within-space consistency $C_W^{\text{in}}$, and finally, the third and fourth rows show the between-space consistency $C_B^{\text{acc}}$ and $C_B^{\rho}$, respectively. The performance is standardized per task, and the sign of AE performance is flipped, similarly to our analysis models.
are not desirable, especially when the transformations we applied are not supposed to have noticeable effects. However, as our consistency investigations showed, the MFCC baseline encoder behaves surprisingly well in terms of consistency, evidencing that hand-crafted features should not always be considered as inferior to deep representations.

While in a conventional audio feature extraction pipeline, important salient data patterns may not be captured due to accidental human omission, our experimental results indicate that DNN representations may be unexpectedly unreliable. In the deep music embedding space, “known relatives” in the audio space may suddenly become faraway pairs. That a representation has certain unexpected inconsistencies should be carefully studied and taken into account, specially given the increasing interest in applying transfer learning using DNN representations, not only in the MIR field. For example, if a system requires to use degraded audio inputs for a pre-trained DNN (which e.g., may be done in music identification tasks), while humans may barely recognize the differences between the inputs and their original form, it does not guarantee that this transformed input may be embedded at a similar position to its original version in a latent space.

6.5. Toward Reliable Deep Music Embeddings

In this work, we proposed to use several distance consistency-based criteria, in order to assess whether representations in various spaces can be deemed as consistent. We see this as a complementary means of diagnosis beyond task-related performance criteria, when aiming to learn more general and robust deep representations. More specifically, we investigated whether deep latent spaces are consistent in terms of distance structure, when smaller and larger transformations on raw audio are introduced (RQ 1). Next to this, we investigated how various types of learning tasks used to train deep encoders impact the consistencies (RQ 2).

Consequentially, we conducted an experiment employing 4 MIR tasks, and considering deep encoders versus a conventional hand-crafted MFCC encoder, to measure the consistency for different scenarios. Our findings can be summarized as follows:

- **RQ 1.** Compared to the MFCC baseline, all DNN encoders indicate lower consistency, both in terms of within-space consistency and between-space consistency, especially when transformations grow from imperceptibly small to larger, more perceptible ones.

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**FIGURE 13** | $C^D_{ij}$ on the original samples, including all the possible distance pairs between audio and latent domain.

**FIGURE 14** | 2-dimensional scatter plot using t-SNE. Each point represents 2-second audio mixture signal chunks that are encoded by a VS-specialized encoder. (A) the color map of points is based on the loudness of the isolated vocal signal for a given mixture signal. The red color indicates higher loudness, and the blue color indicates smaller loudness. (B) the same chunks are colored by the song each chunk belongs to. The samples are randomly sampled from the MUSDB18 dataset.
RQ 2. Considering learning tasks, the high-levelness of a task is correlated with the consistency of resulting encoder. For instance, an AT-specialized encoder, which needs to deal with semantically high-level task, yields the highest within-space consistency, but the lowest between-space consistency. On the other hand, an AE-specialized encoder, which deals with a semantically low-level task, shows opposite trends.

To realize a fully robust testing framework, there still are a number of aspects to be investigated. First of all, more in-depth study is required considering different magnitudes in the transformations, and their possible comparability. While we applied different magnitudes for each transformation, we decided not to comparatively consider the magnitude ranges in the analysis at this moment. This was done, as we do not have any exact means to compare the perceptual effect of different magnitudes, which will be crucial to regularize between transformations.

Furthermore, similar analysis techniques can be applied to more diverse settings of DNNs, including different architectures, different levels of regularizations, and so on. Also, as suggested in Kereliuk et al. [8] and Goodfellow et al. [9], the same measurement and analysis techniques can be used for adversarial examples generated from the DNN itself, as another important means of studying a DNN’s reliability.

Moreover, and based on the observations from our study, it may be possible to develop countermeasures for maintaining high consistency of a model, while yielding high task-specific performance. For instance, unsupervised de-noising such as [35, 36] might be one of the potential solutions. In particular, it can be used when the noise is drawn from the known, relatively simple distribution, such as white noise. However, we also observed some encoders are substantially affected by a very small amount of the noise, which implies even artifacts produced from the denoising algorithm can cause another unexpected inconsistency.

Also, it might not guarantee more musical and structured cases such as tempo or pitch shifts.

For those cases, it can be effective if, during learning, a network is directly supervised to treat transformations in similar ways as their original versions in the latent space. This can be implemented as an auxiliary objective to the main objective of the learning procedure, or introducing directly the transformed examples as the data augmentation.

We believe that our work can be a step forward toward a practical framework for more interpretable deep learning models, in the sense that we suggest a less task-dependent measure for evaluating a deep representation, that still is based on known semantic relationships in the original item space.

**DATA AVAILABILITY STATEMENT**

The datasets generated for this study are available on request to the corresponding author.

**AUTHOR CONTRIBUTIONS**

JK worked on the data generation via running machine learning tasks and wrote the first draft of the manuscript. JU performed the statistical analysis. JK, JU, CL, and AH wrote sections of the manuscript, contributed conception and design of the study, manuscript revision, read, and approved the submitted version.

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**Conflict of Interest:** The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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