Magnetic Energy Transfer and Distribution between Protons and Electrons for Alfvénic Waves at Kinetic Scales in Wavenumber Space

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Abstract

Turbulent dissipation is considered a main source of heating and acceleration in cosmic plasmas. The alternating current Joule-like term, \((\mathbf{j} \cdot \mathbf{E})\), is used to measure the energy transfer between electromagnetic fields and particles. Because the electric field depends on the reference frame, in which frame to calculate \((\mathbf{j} \cdot \mathbf{E})\) is an important issue. We compute the scale-dependent energy transfer rate spectrum in wavevector space, and investigate the electric-field fluctuations in two reference frames: \(\mathbf{E}\) in the mean bulk flow frame and \(\mathbf{E}'\) in the local bulk flow frame (non-inertial reference frame). Considering Alfvénic waves, we find that \((\mathbf{j} \cdot \mathbf{E}')\), which neglects the contribution of work done by the ion inertial force, is not consistent with the magnetic field energy damping rate \((2\gamma \delta B^2)\) according to linear Maxwell–Vlasov theory, while \((\mathbf{j} \cdot \mathbf{E})\) is exactly the same as \(2\gamma \delta B^2\) in wavenumber space \((k_i, k_j)\), where \(\gamma\) is the linear damping rate. Under typical conditions of solar wind at 1 au, we find in our theoretical calculation that the field energy is mainly converted into proton kinetic energy leaving the residual minor portion for electrons. Although the electrons gain energy in the direction perpendicular to the mean magnetic field, they return a significant fraction of their kinetic energy in the parallel direction. Magnetic-field fluctuations can transfer the energy between the parallel and perpendicular directions. Therefore, \((\mathbf{j} \cdot \mathbf{E}')\) and \((\mathbf{j} \cdot \mathbf{E})\) do not solely describe the energy transfer in the parallel direction and perpendicular direction, respectively.

Unified Astronomy Thesaurus concepts: Solar wind (1534); Interplanetary turbulence (830); Alfvén waves (23)

1. Introduction

Turbulence dissipation is an important process in heating and acceleration of particles in extended stellar atmospheres, atmospheres, and the galactic interstellar space. Also the heating of the solar wind is attributed to the dissipation of turbulence. Turbulent dissipation refers to the conversion of turbulent energy into thermal energy or the production of superthermal particle distributions. However, the mechanism of this conversion is not fully understood. In interplanetary turbulence, energy is injected at large scales, cascades to small scales, and dissipates at even smaller (kinetic) scales (Kiyani et al. 2015). Because of the low density of space plasmas, collisionless mechanisms play a vital role in the dissipation (Matthaeus et al. 2015; Chen 2016; Howes 2017).

Resonant damping is suggested as a mechanism for collisionless dissipation. This kind of resonant interaction between particles and electromagnetic (EM) waves in the plasma includes Landau damping, transit-time damping, and cyclotron-resonant damping (Isenberg & Hollweg 1983; Leamon et al. 1998, 1999; Gary 1999; Isenberg 2001; Marsch & Tu 2001; Klein et al. 2017). Observational evidence for Landau damping and cyclotron damping has been reported recently (He et al. 2015a, 2015b). For non-resonant damping, dissipation in coherent structures, such as current sheets (Dmitruk et al. 2004; Osman et al. 2012), discontinuities (Wang et al. 2013; Zhang et al. 2015), and magnetic reconnection at kinetic scales (Drake et al. 2006; Osman et al. 2014), is found both in simulations and observations. Based on the studies by Chen et al. (2001) and Chandran et al. (2010), the stochastic heating of protons is another effective non-resonant mechanism. All of these mechanisms represent an energy transfer from EM fields to particles, accelerating particles and heating the plasma. In the Vlasov description, this energy transfer corresponds to a change in the particle-phase-space density.

The strength of dissipation can be measured by the amount of energy transferred from waves to particles per unit time. This energy transfer is represented by the Joule-like heating term \(\mathbf{j} \cdot \mathbf{E}\) (\(\mathbf{j}\) is the current density and \(\mathbf{E}\) is the electric field) that describes the amount of particle energy gained from the waves per unit time (Stix 1992). The value of \(\mathbf{j} \cdot \mathbf{E}\) depends on the reference frame, in which \(\mathbf{E}\) is evaluated. Zenitani et al. (2011) argue that \(\mathbf{j} \cdot \mathbf{E}'\), where \(\mathbf{E}'\) is the electric field calculated in the local electron bulk flow frame, represents the “true dissipation.” Wan et al. (2015) find that regions of high current density usually have high \(\mathbf{j} \cdot \mathbf{E}'\) in their 3D plasma turbulence simulation. Birn & Hesse (2010) further argue that the plasma heating is contributed by both \(\mathbf{j} \cdot \mathbf{E}'\) and the work of the pressure gradient force \((\mathbf{P} \cdot \nabla)\) for plasma heating. The pressure tensor also plays a role for changing the fluid entropy in the dissipation (Du et al. 2020).

In the fast solar wind, Alfvénic fluctuations dominate the magnetohydrodynamic (MHD) scales (Belcher & Davis 1971). At kinetic scales, turbulence may consist of fluctuations that behave like kinetic Alfvén waves (KAWs), Alfvén cyclotron waves, or whistler waves (Galtier & Bhattacharjee 2003; Bale et al. 2005; Sahraoui et al. 2009; Schekochihin et al. 2009; Gary et al. 2012; He et al. 2012). In addition, the distribution of turbulent energy is anisotropic with \(k_i \ll k_j\) in wavenumber space \((k_i, k_j)\) space; Goldreich & Sridhar 1995; Horbury et al. 2008; Podesta 2009; Chen et al. 2010). Narita & Gary (2010) and Sahraoui et al. (2010) show the anisotropy of the power spectral density (PSD) \((k_i, k_j)\) around the ion kinetic range by applying the k-filtering method to Cluster data. He et al. (2013) develop a tomography...
method to reconstruct the multi-dimensional PSD of magnetic field from data of Helios 2, which reveals an oblique ridge of PSD closer to the $k_\perp$ axis than to the $k_P$ axis. Yan et al. (2016) employ the same method as He et al. (2013) and discover the anisotropy of the residual energy $E_{Ervb} = E_{vv} - E_b$, which is distributed along the $k_\perp$ axis and concentrates at very small $k_P$. The anisotropy of turbulence energy in wavenumber space may be caused by the cascade of Alfvén waves preferentially in the perpendicular direction, or by intermittency (Wang et al. 2014; Pei et al. 2016). Most previous turbulence studies focus on the analysis of magnetic-energy spectra, yet the EM energy-conversion-rate spectra have been scarcely investigated and remain unknown. He et al. (2019a) measure the EM energy-conversion rate spectra in magnetosheath turbulence, and find that it is enhanced around the ion kinetic scales. On the other hand, the EM energy-conversion rate can also be used to identify the wave excitation and growth, which is a prevalent phenomenon in the foreshock region (He et al. 2019b). In this work, we theoretically predict the energy-conversion-rate spectra around the proton kinetic range for Alfvénic waves and compare these spectra between different reference frames. We discuss the interpretation and implications of our work in Section 4.

2. Energy Transfer of Alfvénic Modes in Kinetic Theory

We assume the plasma to consist of only protons and electrons, without background electric field and bulk flow velocity. Both species of particles are isotropic and Maxwellian without drifts. We assume $m_p/m_e = 1836, \beta_{p\parallel} = \beta_{p\perp} = \beta_e = \beta_e = 1$, and $v_A/c = 0.00016$. We adopt the numerical New Hampshire Dispersion Relation Solver code (Verscharen & Chandran 2018) to calculate the dispersion and polarization relations of wave modes in wavenumber space based on the linearized set of the Vlasov–Maxwell equations. We take the background magnetic field $B_0$ along the $z$ direction, and the wavevector $k$ to be in the $x$–$z$ plane ($k = (k_\perp, 0, k_\parallel)$). The frequency of waves is normalized to the proton gyrofrequency $\Omega_p = eB_0/m_p$, and fields are scaled to $\delta B_e$. Around the ion scale ($k\rho_p \sim 1, \rho_p = v_{th,p}/\Omega_p$ is the proton thermal gyroradius), the Alfvénic mode transitions into the KAW for quasi-perpendicular propagation or the ion cyclotron wave (ICW) for quasi-parallel propagation.

From the second moment of the Vlasov equation ($W_e = (m_e/2) \iint v^2 f_e dv_x dv_y dv_z$ is the total kinetic energy and $Q_e = (m_e/2) \iint v^2 f_e dv_x dv_y dv_z$ is the total kinetic-energy flux...
where the index $s = p$ represents protons and the index $s = e$ represents electrons. Particles gain energy from the electromagnetic field through the $j \cdot E$ term ($j = j_p + j_e$). We use the distribution of $\delta j$ and $\delta E$ in wavenumber space to build $\delta j \cdot \delta E$ spectra ($\delta$ represents the fluctuating part of a quantity). The average energy transfer rate over a few periods is given by (Stix 1992):

$$\langle \delta j \cdot \delta E \rangle = \frac{1}{4} \langle \delta j^* \cdot \delta E + \delta j \cdot \delta E^* \rangle,$$

where the asterisk indicates the complex conjugate. Note that $\delta E$ and $\delta E^*$ in Equation (2) are the Fourier amplitudes of the electric field in the plasma frame (or mean bulk flow reference frame), which is an inertial reference frame. When transforming into the local bulk flow reference frame, the electric field can be expressed as $\delta E' = \delta E + \delta v \times (B_0 + \delta B_0)$, thus additional inertial forces arise. In the solar wind, the EM energy is dominated by the energy of the magnetic-field fluctuations. Using the damping rate $\gamma$ (the imaginary part of the wave frequency), we write the magnetic-energy damping rate as:

$$\frac{d\delta W_B}{dt} = \frac{\gamma}{2\mu_0} \delta B^2 = 2\gamma \delta W_B,$$

where $\delta W_B = \delta B^2/(2\mu_0)$ is the energy of the fluctuating magnetic field. The dispersion relation of the Alfvén wave branch is shown in Figure 1. The real part of the frequency, $\omega$, increases with $k_\parallel$, while $\omega/k_\parallel$ increases with $k_\perp$ as expected. The dispersion relations at $k_\parallel(\rho_p + d_p) \sim 1, k_\perp(\rho_p + d_p) \sim 0)$ and $(k_\parallel(\rho_p + d_p) \sim 0, k_\perp(\rho_p + d_p) > 1)$ represent the characteristics of ICWs and KAWs, respectively. We define the effective damping rate:

$$\gamma_{\text{eff}} = \frac{-\langle \delta j \cdot \delta E \rangle}{2\delta W_B},$$

which describes the ratio of $\langle \delta j \cdot \delta E \rangle$ to the fluctuating magnetic field energy. If $\gamma_{\text{eff}} < 0$, the EM energy is converted to particle kinetic energy; if $\gamma_{\text{eff}} > 0$, the EM fields receive energy from the particles. Figure 2 shows that the effective damping rate is equal to the wave damping rate. The coordinates in the figures are expressed as $k_\parallel(\rho_p + d_p)$, where $d_p = v_A/\Omega_p$ is the proton inertial length. For the case of $k = k_\parallel$, this scale refers to the proton cyclotron resonance (Leamon et al. 1998), and this resonance may contribute to the break between the inertial range and...
dissipation range in the magnetic field PSD of solar-wind turbulence (Wang et al. 2018; Woodham et al. 2018; Duan et al. 2018). The behavior of the effective damping rate illustrates that the fluctuating magnetic energy fully converts to particle kinetic energy through the $\dot{j} \cdot E$ term. It also indicates the validity of using $\dot{j}$ and $\delta E$ to estimate the spectrum of energy conversion. The magnetic field energy damps quickly around $k (\rho_p + d_p) = 1$, where the normalized damping rate $\gamma/\Omega_p$ approaches $-0.1$.

In the local bulk flow reference frame, the distribution of the effective damping rate in wavenumber space is different from that in the mean bulk flow reference frame. Panels (b) and (c) in Figure 3 show the effective damping rate in the local proton and electron bulk-flow reference frame ($v_{\text{ref}} = \delta v_p$ or $\delta v_e$). These two panels are identical, because $\dot{j} \cdot (\delta E'_p - \delta E'_e) = \delta j \cdot [(\delta v - \delta v_p) \times B_0] = \delta j \cdot (\delta j \times B_0) = 0$, where $\delta E'_p$ and $\delta E'_e$ are the fluctuating electric field in the reference frames of $v_{\text{ref}} = \delta v_p$ and $v_{\text{ref}} = \delta v_e$, respectively. The fluctuating current and magnetic field do not change in the frame transformation, since we assume $\delta v_p$ and $\delta v_e$ to be much smaller than the speed of light. Compared to the mean bulk flow frame (panel (a)), the effective damping rate is much smaller. It means the $\langle \dot{j} \cdot \delta E' \rangle$ is much smaller in the local bulk flow frame, as shown by Wan et al. (2015). The work done by the inertial force in the non-inertial frame (local bulk flow frame) is responsible for this imbalance. If we choose a periodically varying velocity as a reference velocity, the frame is by definition non-inertial. The work done by the resultant inertial force and its contribution to the energy transfer balance will be discussed in detail in Section 4. Moreover, $\delta E' = \delta E + \delta v_{\text{ref}} \times B$ serves as a measure for the frozen-in condition. At large scales, waves follow the frozen-in condition, so that $\delta E' \approx 0$, and $\dot{j} \cdot \delta E' \approx 0$ in the region of small $k$ (see Figure 3). At larger $k$, however, $\delta E' \approx 0$ and $\dot{j} \cdot \delta E' \approx 0$, indicating that the frozen-in condition is broken at small scales as expected.

3. Energy Distribution between Protons and Electrons

We now divide the fluctuating current into current populations carried by different species ($\dot{j}_s = n_s q_s \delta v_s$). The $\dot{j}_s \cdot E$ term describes the amount of energy that is converted to protons and electrons separately. Figure 4 shows the scale-dependent effective damping rate $\gamma_{\text{eff}}$ for protons and electrons, respectively. Protons receive most of the EM energy, and their effective damping rate increases along $k_p$. Electrons receive almost no energy at small $k$. In the range of $k (\rho_p + d_p) \sim 1$,
\( \gamma_{\text{eff},e}/\Omega_p \) assumes a small and positive value, which means electrons transfer a small proportion of their kinetic energy to the EM fields. There are two possible explanations for why \( \langle j \cdot E \rangle \) can vanish. One is that the vectors \( j \) and \( E \) are orthogonal to each other all the time, another is that the average of \( j \cdot E \) over multiple periods is equal to zero. In the MHD Alfvénic range, the fluctuating electric field is perpendicular to the fluctuating velocity, so the effective damping rate in this region is zero. At smaller scales, however, kinetic effects introduce phase differences other than 90°.

As \( \langle \delta j \cdot \delta E \rangle = \langle \delta j \cdot \delta E_\parallel \rangle + \langle \delta j \cdot \delta E_\perp \rangle \), the effective damping rates allow us to decompose the energy transfer between the parallel and perpendicular degrees of freedom. We show this separated distribution in wavenumber space in Figure 5. The protons gain more energy along the perpendicular direction than along the parallel direction, which is the result of cyclotron-resonant wave-particle interactions. \( \gamma_{\text{eff},||}/\Omega_p < -0.01 \) in the region \( k_\parallel (\rho_p + d_p) > 0.6, k_\perp (\rho_p + d_p) > 0.3 \), which may be related to the energy transfer via Landau damping of KAWs along the parallel direction. The distributions of \( \gamma_{\text{eff},||}/\Omega_p \) and \( \gamma_{\text{eff},\perp}/\Omega_p \) display an opposite pattern in wavenumber space. This opposite pattern suggests that particles are scattered in pitch-angle during the damping process. We quantify this effect by separating the kinetic-energy Equation (1) into two kinetic-energy equations relating to the parallel and perpendicular kinetic energies as:

\[
\frac{\partial \delta W_\parallel}{\partial t} + \nabla \cdot \delta \mathbf{Q}_\parallel = \delta \mathbf{E}_\parallel \cdot \delta j_\parallel + q_i \int \int \int (v_i \delta B_x - v_i \delta B_y) \delta f_i \, dv_x \, dv_y \, dv_z \\
\frac{\partial \delta W_\perp}{\partial t} + \nabla \cdot \delta \mathbf{Q}_\perp = \delta \mathbf{E}_\perp \cdot \delta j_\perp + q_i \int \int \int (v_i \delta B_x - v_i \delta B_y) \delta f_i \, dv_x \, dv_y \, dv_z,
\]

where \( \delta W_\parallel = \langle m_i \rangle_\parallel / 2 \int \int (v_x^2 + v_y^2) \delta f_i \, dv_x \, dv_y \) and \( \delta W_\perp = \langle m_i \rangle_\perp / 2 \int \int (v_x^2 + v_y^2) \delta f_i \, dv_x \, dv_y \) are the kinetic energies associated with the particle velocity in the parallel and perpendicular directions separately. Since we do not consider relative drifts in the mean flow frame, particle kinetic energy is directly associated with thermal energy in our case. The lhs of Equations (5) and (6) represent the parallel and perpendicular energy transfer rates, which may be caused by Landau damping (parallel) and cyclotron damping (perpendicular) of EM energy. The Lorentz force leads to a transfer between the parallel and perpendicular degrees of freedom (rhs of Equations (5) and (6)), but it does not increase the total kinetic energy. Therefore, \( \langle \delta \mathbf{E}_\parallel \cdot \delta j_\parallel \rangle \) and \( \langle \delta \mathbf{E}_\perp \cdot \delta j_\perp \rangle \) are not necessarily
direct measures for Landau damping and cyclotron damping under general conditions for waves with arbitrary propagation angle. This scenario of energy transfer is shown in Figure 6.

4. Summary and Discussion

In this study, we compute the EM energy-conversion rate spectra in wavenumber space. We define the effective damping rate $\gamma_{\text{eff}}$, as the ratio of converted energy to magnetic field energy. Comparing the effective damping rate in the mean flow frame and local (oscillating) flow frame, we find that $\langle \delta \mathbf{j} \cdot \delta \mathbf{E} \rangle$ does not appropriately reflect the transfer of energy between fields and particles, while $\langle \delta \mathbf{j} \cdot \delta \mathbf{E} \rangle$ is consistent with the damping rate of magnetic field energy. In the large $k$ region around ion scales, most of the EM-field energy is converted into proton kinetic energy rather than electron kinetic energy.

The energy partitioning between protons and electrons depends on various parameters, e.g., fluctuation amplitude, plasma $\beta$, and temperature ratio ($T_i/T_e$). Our study focuses on the ion scale under the typical solar-wind conditions at 1 au. At smaller scales (electron scales), electrons receive more energy than protons via electron Landau damping of obliquely propagating KAWs (Leamon et al. 1999). Kinetic simulations show that the total heating rate of electrons increases relative to...
the heating rate of protons when both ion and electron kinetic scales are taken into account (Matthaeus et al. 2016). The application of our method to conditions with low ion plasma $\beta_i$ ($\beta_i = 0.1$) can help to understand the Parker Solar Probe (PSP) measurements in the inner heliosphere in a future project; however, a detailed study of these conditions is beyond the scope of this work.

In addition, the $\langle j \cdot E' \rangle$ term only describes the conversion between EM-field energy and particle kinetic energy, and does not provide information about the conversion between bulk kinetic energy and thermal kinetic energy. When transformed between different reference frames, the velocity distribution function just shifts as a whole in velocity space. Both $\delta E$ and $\delta E'$ work on all of the particles, so they only contribute to the energy transfer into bulk kinetic energy. There is no direct energy transfer from EM energy to thermal energy. However, for the dissipation of Alfvénic turbulence, both fluctuating EM-field energy and fluctuating bulk kinetic energy will eventually be dissipated and converted into thermal kinetic energy.

The power associated with the inertial force for a particle species depends on the amplitude of the velocity fluctuation, the wave frequency, and the mass of a particle of the given species: $P_{\text{inertial}} = -m_i \frac{d^2 v_{bs}}{dt^2} \cdot \nabla _v$. The effect of the inertial force becomes more significant at smaller scales, as $\omega$ increases with decreasing scale. Its effect on electrons may be neglected compared to that on protons because the electron mass is much smaller than the proton mass. In the guiding center approximation, the inertial force can be expressed as the polarization drift, which is more important for protons than for electrons in simulations (Li et al. 2018, 2019).

There is a possible way to include $\delta j \cdot \delta E'$ in the governing equation for thermal kinetic energy. Substituting $E' = E + v_{bs} \times B$ into the momentum equation ($\dot{v}_{bs}$ is the bulk flow velocity of species $s$), leads to

$$n_s m_s \frac{d v_{bs}}{dt} = n_s q_s (E + v_{bs} \times B) - \nabla \cdot P_s.$$  

(7)

Multiplying the equation with $v_{bs}$ yields

$$v_{bs} \cdot (\nabla \cdot P_s) = n_s q_s v_{bs} \cdot E' - n_s m_s v_{bs} \cdot \frac{d v_{bs}}{dt} = \dot{j}_s \cdot E' - n_s m_s v_{bs} \cdot \frac{d v_{bs}}{dt}.$$  

(8)

The term $n_s m_s v_{bs} \cdot \left( \frac{d v_{bs}}{dt} \right)$ is the rate of change of bulk kinetic energy. In the non-inertial frame, this is the power due to the inertial force to guarantee energy conservation. Substituting this term into the thermal energy equation ($W_{\text{th, s}} = (m_i/2) \int (\mathbf{v} - v_{bs})^2 f_i d\mathbf{v}_i d\mathbf{v}_e$ is the particle thermal energy) leads to

$$\frac{\partial W_{\text{th, s}}}{\partial t} + \nabla \cdot (W_{\text{th, s}} v_{bs} + h_s + P_s \cdot v_{bs}) = \dot{j}_s \cdot E' - n_s m_s v_{bs} \cdot \frac{d v_{bs}}{dt},$$  

(9)

where $h_s = (m_i/2) \int (\mathbf{v} - v_{bs})^2 f_i d\mathbf{v}_i d\mathbf{v}_e$ is the heat flux vector. We note that in association with the appearance of $\dot{j}_s \cdot E'$, the power associated with the inertial force also exists in Equation (9). These derivations show that $j \cdot E'$ cannot fully describe the energy transfer to particle thermal energy, except if $n_s m_s v_{bs} \cdot \left( \frac{d v_{bs}}{dt} \right) = 0$. The combination of $j \cdot E'$ and $n_s m_s v_{bs} \cdot \left( \frac{d v_{bs}}{dt} \right)$, which is the same as $v_{bs} \cdot (\nabla \cdot P_s)$, must be taken into consideration. Whether the energy transfer between EM fields and particles ($\sum_i \dot{j}_i \cdot E_i$) is less or greater than the energy transfer between bulk kinetic energy and thermal kinetic energy ($\sum_i (P_i \cdot \nabla) \cdot v_{bs}$) is another interesting question to be addressed in the future through theoretical calculation and observational analysis. Yang et al. (2019) find that the scale-dependent $- (P_i \cdot \nabla) \cdot v_{bs}$ dominates the energy conversion at smaller scales in their 2.5D kinetic simulations.

The exact contributions of Landau and cyclotron resonances are difficult to estimate. For example, $\langle j_{\parallel} \cdot E \rangle$ represents the total rate of energy conversion in the perpendicular direction, including the contributions from the particles satisfying the cyclotron-resonance condition and other particles outside the resonant velocity range, as long as they carry part of the current $j_{\parallel}$. On the other hand, the particle scattering in phase space due to cyclotron resonance is also governed by the Lorentz force of the fluctuating magnetic field, which transfers energy between perpendicular and parallel degrees of freedom, and acts together with the electric force to form the diffusion plateau of cyclotron resonance in phase space. For $\langle j_{\parallel} \cdot E \rangle$, the situation similarly consists of both a Landau resonance part and a non-resonant part. Like in the cyclotron-resonant case, its strength depends on the distribution of the particle-phase-space density. At small $\beta_i j_{\parallel}$ (the angle between $B_0$ and $k$) and large scales, the effect of ion cyclotron resonances is presumably stronger because the resonance condition is easier to satisfy. At larger $\beta_i j_{\parallel}$ and smaller scales, Landau damping plays a more important role (Leamon et al. 1999).

Our results show a significant energy transfer around the scale $k_i (\rho_i + d_i) \sim 1$. This scale is related to the proton cyclotron resonance, which may lead to the spectral break observed in the magnetic-field power spectra in solar-wind turbulence (Duan et al. 2018, 2020). The spectral break may also be caused by the transition of Alfvénic turbulence to dispersive Alfvénic turbulence around the ion scale. Future work is planned to compute the energy-conversion rate spectrum based on in situ measurements in space, and investigate its relation to the underlying physical processes of diffusion, dissipation, and dispersion in the evolving solar-wind streams will be one of the key issues when investigating the solar-wind turbulence measurements from PSP (He & Tian 2019).

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