Environmental Enhancement of DM Haloes

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Abstract. We study the properties of dark matter haloes of a LCDM model in different environments. Using the distance of the 5th nearest neighbour as an environmental density indicator, we show that haloes in a high density environment are more massive, richer, have larger radii and larger velocity dispersions than haloes in a low density environment. Haloes in high density regions move with larger velocities, and are more spherical than haloes in low density regions. In addition, low mass haloes in the vicinity of the most massive haloes are themselves more massive, larger, and have larger rms velocities and larger 3D velocities than low mass haloes far from massive haloes. The velocities of low mass haloes near massive haloes increase with the parent halo mass. Our results are in agreement with recent findings about environmental effects for groups and clusters of galaxies from deep (SDSS and LCRS) surveys.

Keywords: Cosmology: simulations – cosmology: large-scale structure of the Universe.

1. Introduction

Recent analyses of deep redshift surveys of galaxies, as the Las Campanas Redshift Survey (LCRS), the Sloan Digital Sky Survey (SDSS) and the two-degree-field (2dF) Galaxy Redshift Survey have demonstrated the presence of environmental enhancement of groups and clusters of galaxies – groups and clusters of galaxies in high density regions are richer, more massive, more luminous and have larger velocity dispersions than groups and clusters of galaxies in low density regions (Einasto et al. 2003a, 2003b, 2003c, 2003d, Ragone et al. 2004).

The goal of the present paper is to study the properties of dark matter (DM) haloes in LCDM simulations in various environments and to compare the properties of these haloes with observational results for groups and clusters of galaxies.

In the next Section we describe the numerical model and the halo finding procedure used in our analysis. Then we describe the method to calculate environmental densities around haloes, and study the properties of haloes in different environments. In the last two Sections we give a discussion and summary of our results.

The colour figures and the three-dimensional distribution of the simulated haloes can be seen at the home page of Tartu Observatory (http://www.aai.ee/~maret/cosmoweb.html), where we also present a catalogue of DM halos.

2. The N-body model and the DM haloes

For the present study we use a flat cosmological model with the parameters obtained from the WMAP microwave back-ground anisotropy experiment (Bennett et al. 2003): the total matter density \( \Omega_m = 0.27 \), the baryonic density \( \Omega_b = 0.044 \), the vacuum (dark) energy density (the cosmological constant) \( \Omega_\Lambda = 0.73 \), the Hubble constant \( h = 0.71 \) (here and throughout this paper \( h \) is the present-day Hubble constant in units of 100 km s\(^{-1}\) Mpc\(^{-1}\)) and the rms mass density fluctuation parameter \( \sigma_8 = 0.84 \).

The simulations were performed using the Multi Level Adaptive Particle Mesh code (MLAPM, Knebe et al. 2001). This code uses adaptive mesh techniques and adaptive force softening; new sub-grids are created in regions where the density exceeds a specified threshold. This scheme allows to improve considerably the spatial resolution of the particle-mesh code without loss in the mass resolution, similarly to the ART code (Kravtsov and Klypin 1997). It is known that two-particle relaxation may enhance the fraction of particles in clusters. Adaptive force softening is found to prevent mass segregation caused by two-body relaxation, while in other algorithms (etc. GADGET), based on fixed force softening, two-body relaxation is more prominent (Binney and Knebe 2002).

We use the results of a simulation run in a cube of 200 h\(^{-1}\) Mpc size, using a 256\(^3\) mesh and the same number of particles. Each particle has a mass of \( 3.57 \times 10^{10} h^{-1} M_\odot \). The transfer function was computed using the COSMICS code by E. Bertschinger (http://arcturus.mit.edu/cosmics/).

For selection of dark matter haloes we used the FoF (Friends-of-Friends) algorithm (Zeldovich, Einasto, and Shandarin 1982).

We shall use the linking length 0.23 in units of the mean particle separation, which approximately corresponds to the matter density contrast \( \delta n/n = 80 \). This value was used in compiling the catalogue of the Las Campanas Loose Groups...
of Galaxies, hereafter LCLG (Tucker et al. 2000; Heinämäki et al. 2003). It is substantially lower than the spherical collapse model prediction for virialized objects, $\delta n / n = 178 \Omega_m^{-0.6}$ (White, Efstathiou and Frenk 1993).

Too large a linking length may lead to overestimation of the masses of the simulated groups since particles outside of the virialized core are included in the groups. To avoid possible effects of unbound groups in simulations, we used the virial condition $E_r = E_{\text{kin}} / |E_{\text{pot}}| < 0.5$ ($E_{\text{pot}}$ is the potential energy and $E_{\text{kin}}$ the kinetic energy of a group) for groups to be included in our final group catalogue. Moreover, to avoid too small groups we choose only groups which included more than 100 dark matter particles, imposing a minimum halo mass of $3.57 \times 10^{12} h^{-1} M_{\odot}$. The catalogue contained 5355 dark matter haloes, and after applying the virial condition, 5219 dark matter haloes remained in our final catalogue.

Fig. 1 shows the cumulative mass function for dark matter haloes, compared with observational data (LCLG). The mass function of the LCLG (with Poisson error bars) is shown by filled circles. For a more detailed description of selection effects in the LCLG sample, see Tucker et al. (2000) and Heinämäki et al. (2003). The solid line shows the mass function for haloes; the filled circles show the LCLG result and the solid line describes our simulations.

3. Haloes in different environments

3.1. Environmental densities around haloes

In the present work we determine spatial densities around haloes, using the distance to the halo’s 5th neighbour halo. We shall use this distance as an environmental parameter. When we use this distance as the density indicator, we always see the characteristic scales of the features we study. This method has been used before to find environmental (projected or spatial) densities around galaxies (Caon and Einasto 1995, Goto et al. 2003a, b) around clusters (Schuecker et al. 2001; Einasto et al. 2004a) and even around superclusters of galaxies (Einasto et al. 1997).

Using the 5th neighbour distance we shall divide the haloes into four environment regions as described in Table 1. The neighbour distance intervals are chosen to have approximately the same number of haloes in each region. The region H23.1 has the closest neighbours and the highest environmental densities, the class H23.4 has the most distant neighbours and the lowest environmental densities.

3.2. Two richness classes of haloes

In Einasto et al. (2003c) we showed that the properties of the LCLGs in the neighbourhood of rich clusters are enhanced in comparison with the properties of the LCLGs in average. Moreover, in Einasto et al. (2003c) we showed that the LCLGs in superclusters are more massive than loose groups of galaxies that do not belong to superclusters.

To test this result using LCDM haloes, we divided our sample of LCDM haloes into two richness classes: the most massive haloes that correspond to rich clusters of galaxies, and less massive haloes that correspond to loose groups of galaxies. Here we used the mass threshold $M \geq 6.3 \times 10^{13} h^{-1} M_{\odot}$ (see Heinämäki et al. 2003). Einasto et al. (2003c) also used this threshold to determine the population of Abell-class clusters among the LCLGs.

Once two subsamples with different masses were determined, we found for the most massive haloes their 5 closest neighbours among less massive haloes (with masses $M < 6.3 \times 10^{13} h^{-1} M_{\odot}$). Then we divided the population of low mass neighbours into the populations of close neighbours (CN) and distant neighbours (DN), using a threshold distance of 6 $h^{-1}$ Mpc. This distance was used in Einasto et al. (2003c) to define the populations of loose groups around rich clusters of galaxies.

4. The properties of haloes in different environment

4.1. Haloes in high and low density regions

The spatial distribution of haloes in our $L = 200 h^{-1}$ Mpc simulation box is shown in Fig. 2 (a 50 $h^{-1}$ Mpc thick slice in the Z-direction; color figures of all slices are given in our web page together with animations). This figure shows haloes located in regions of different densities, as quantified by the 5th nearest neighbour distance. In general, in high density regions haloes are bigger and more massive than haloes located in low density regions. The velocities of haloes in high density regions are also larger than the velocities of haloes in low density regions. The velocity vectors of haloes are directed toward rich filaments and massive haloes – mass flows from voids into filaments, which act as attractors. In extreme void regions, where the haloes are most isolated, the haloes almost do not move; they also have low masses.
Fig. 2. The spatial distribution of haloes in regions of different density in a slice of thickness of 50 \( h^{-1} \) Mpc (in the Z-direction); the Z interval is 150–200 \( h^{-1} \) Mpc. The left panel shows the spatial distribution of haloes, the right panel shows the velocity vectors of haloes. Filled large circles denote haloes in the highest density environment (sample H23.1 in Table 1), filled small diamonds stand for the sample H23.2, open circles for the sample H23.3, and crosses denote haloes in the lowest density environment, sample H23.4.

Table 1. Median and upper quartile (in parentheses) values of halo properties in high and low density environments.

| Sample     | \( N_{\text{halo}} \) | \( D_1(5N) \) | \( D_2(5N) \) | \( N_p \) | \( \log M_{\text{vir}} \) | \( R_v \) | \( \sigma \) | \( V \) | \( E \) | \( N_M \) |
|------------|------------------------|----------------|----------------|------|------------------------|------|------|------|------|------|
| H23.1      | 1315                   | 0.0            | 7.9            | 409  | (992)                  | 12.70| (13.17)| 0.40 | (0.51)| 240  | (380)| 480  | (640)| 0.50 | (0.63)| 101  |
| H23.2      | 1287                   | 7.9            | 9.7            | 357  | (816)                  | 12.59| (13.04)| 0.38 | (0.50)| 210  | (340)| 445  | (585)| 0.51 | (0.65)| 66   |
| H23.3      | 1340                   | 9.7            | 12.2           | 309  | (651)                  | 12.49| (12.92)| 0.37 | (0.46)| 190  | (300)| 400  | (535)| 0.50 | (0.64)| 37   |
| H23.4      | 1280                   | 12.2           |                | 247  | (463)                  | 12.32| (12.70)| 0.36 | (0.44)| 160  | (250)| 345  | (470)| 0.52 | (0.66)| 18   |

The columns in the Table are as follows:

- column 1: the halo sample number,
- column 2: the number of haloes in the sample,
- column 3: the smallest 5th nearest neighbour distance,
- column 4: the largest 5th nearest neighbour distance,
- column 5: the number of particles in a halo,
- column 6: the virial mass of a halo (log), \( M_{\text{vir}} = \sigma^2 R_v / G \),
- column 7: the virial radius of a halo (for equal mass particles), \( R_v = N^2 / (\sum_{\text{pairs}} s_{ij}) \),
- column 8: the rms velocity of halo particles, \( \sigma = \sqrt{\sum v_i^2 / N} \), where the squared velocity deviation \( v_i^2 = (v_{i,x} - v_{c,x})^2 + (v_{i,y} - v_{c,y})^2 + (v_{i,z} - v_{c,z})^2 \) is relative to the mean velocity of the halo and \( v_{c,x}, v_{c,y}, v_{c,z} \) are the components of the mean velocity.
- column 9: the velocity of a halo, \( v_{\text{halo}} = \sqrt{v_{c,x}^2 + v_{c,y}^2 + v_{c,z}^2} \),
- column 10: the eccentricity of a halo, \( \varepsilon = 1 - cc/aa \), where \( cc \) is the semi-minor axis and \( aa \) is the semi-major axis.
- column 11: the number of haloes with masses \( M \geq 6.3 \times 10^{13} h^{-1} M_{\odot} \).

Let us now analyse the properties of haloes in various environments in more detail. We made a series of scatter plots, in which we plotted the number of particles in haloes, halo’s virial radii, masses and velocity dispersions against the distance of the 5th nearest neighbour of the halo, and calculated cumulative distributions of these parameters (the number of particles in haloes, halo’s virial radii, masses and velocity dispersions) for haloes from different environments, and the median and upper quartile values of the properties of haloes from high and low density regions. We have also estimated the statistical significance of our results, using the Kolmogorov-Smirnov test.

We compare haloes from different environments in Table 1. The columns show median and upper quartile (in parentheses) values of halo properties in high and low density environments. In order to not overcrowd the paper with figures, we show only one scatter plot, for the halo richness (Fig. 3). Fig. 3 and Table 1 show that the properties of haloes in high density regions are environmentally enhanced: they are...
Fig. 3. The number of particles in haloes versus the distance of the 5th nearest neighbour of the halo.

richer, larger, more massive, and have larger velocity dispersions than haloes in low density regions. The haloes in high density regions have larger velocities than haloes in a low density environment. In the lowest density regions (low density filaments and voids) haloes almost do not move. This is seen also in Fig. 4.

The cumulative mass function (MF) is defined as the number density of clusters/groups above a given mass $M$, $n(M)$. We used the same definition also for other properties of the haloes. Thus we get the cumulative richness distribution, the cumulative virial radius distribution, the cumulative rms velocity distribution, and the cumulative peculiar velocity distribution. We plot these functions for haloes in different environments in Fig. 4. These figures and Table 1 show that haloes in a high density environment are richer, they have larger masses, larger radii, larger rms velocities and larger peculiar velocities than haloes in a low density environment. For example, at the density level $10^{-6} h^3 \text{Mpc}^{-3}$ the H23.1 clusters are about 3 times richer than the H23.4 clusters. The cluster class haloes (with mass $M \geq 6.3 \times 10^{13} h^{-1} M_{\odot}$) are preferentially located in high density regions. A few cluster class haloes, however, are located in lower density environments. This is due to the selection procedure of the haloes – the most massive haloes do not have very close neighbours (they are halo’s members), thus the local density is suppressed in the neighbourhood of the halo. This is seen also in colour figures in our web page.

We have determined also the eccentricities of DM-haloes. Fig. 5 and Table 1 hint at the trend that the eccentricities of haloes in high density regions seem to be smaller than the eccentricities of haloes in low density regions. Haloes in high...
density regions are more spherical than haloes in low density regions, an evidence of a higher degree of virilization.

Fig. 5 shows also, that the differences between the eccentricities of haloes from different environments are smaller than the differences between other parameters (distributions on the Fig. 5 left panel, for samples H23.2 and H23.3 even practically overlap). The reason for that can be seen in the right panel of Fig. 5: haloes of medium richness (about 200 – 1000 particles, mass \( \leq 3.57 \times 10^{13} M_\odot \)) have smaller eccentricities. This is probably due to several factors: haloes of medium richness are more evolved than very poor haloes, this makes them more spherical. The shape of the richest haloes is more elongated due to the influence of the large scale structure around them (filaments). The environmental dependence of the shapes of haloes is affected by these factors and is thus weaker than other environmental dependences.

The Kolmogorov-Smirnov test shows that the differences between the parameters of haloes from high and low density regions are statistically significant at the 99% significance level for all parameters except eccentricities. The differences between eccentricities of haloes in the highest and the lowest density regions are statistically significant at the 75% significance level according to the Kolmogorov-Smirnov test.

4.2. Properties of haloes in the neighbourhood of the most massive haloes

In Table 2 we give the median and upper quartile values of the parameters of the halo populations CN and DN (close neighbours and distant neighbours, see Sect. 3.2). In Fig. 6 we show the cumulative richness distributions, the mass functions, the cumulative virial radius distributions, and the cumulative peculiar velocity distributions for low mass haloes around high mass haloes. In Table 4 we also give the statistical significances of the differences between the samples, according to the Kolmogorov-Smirnov test.

Fig. 5 and Table 2 show that the low mass haloes in the close neighbourhood of high mass haloes are themselves richer, more massive, have larger rms velocities and move faster than the low mass haloes far from massive haloes. The eccentricities of haloes in the neighbourhood of massive haloes are smaller than the eccentricities of haloes farther away from massive haloes.

We also checked whether the properties of low mass haloes in the vicinity of massive haloes depend on the masses of high mass haloes. Our calculations show that while the intrinsic properties of low mass haloes do not seem to depend on the mass of the parent massive halo, peculiar velocities of low mass haloes in the vicinity of massive halo increase with the parent halo mass (Fig. 4 left panel) – an indication of the gravitational influence of massive haloes.

We obtain similar results if we use summed particle masses instead of virial masses for the massive haloes.

Our calculations show that if we find all low mass neighbours around high mass haloes within a \( 6 h^{-1} \) Mpc sphere, (not just 5 closest neighbours), then we obtain almost the same population (with about 470 member haloes) of low mass neighbours. Thus we used the five closest neighbours, in accordance with our definition of environmental densities around haloes.

5. Discussion

5.1. Comparison with observations

Already early studies of galaxies in different environments showed the presence of strong morphology-density and luminosity-density relations (Dressler 1980, Postman & Geller 1984, Einasto & Einasto 1987, Einasto 1991a and 1991b, Mo et al. 1992). Presently, these relations are studied intensively, using new deep surveys of galaxies (Norberg et al. 2001, 2002, Croton et al. 2004, Kauffmann et al. 2004, Balogh et al. 2004, and Blanton et al. 2004 among others).

However, the study of the properties of galaxy groups and clusters in various environments is only in the beginning.
Fig. 6. The cumulative distributions of various parameters for low mass haloes in the vicinity of the most massive haloes. Upper left panel: cumulative richness. Upper right panel: the mass functions. Lower left panel: the cumulative rms velocity. Lower right panel: the cumulative peculiar velocity. Solid line — close neighbours, the sample CN, dashed line — distant neighbours, the sample DN.

Table 2. Median and upper quartile (in parentheses) values of the properties of low mass haloes in the neighbourhood of massive haloes.

| Sample | $N_{\text{halo}}$ | $D_1(N5)$ | $D_2(N5)$ | $N_p$ | log $M_{\text{vir}}$ | $R_c$ | $\sigma$ | $V_{\text{pec}}$ | $E$ |
|--------|-----------------|------------|------------|-------|---------------------|-------|--------|----------------|-----|
| CN     | 450             | 0.0        | 6.0        | 395   | (774)               | 12.73 | (13.07) | 0.40 (0.50)   | 240 | (340) | 600 (770) | 0.51 (0.62) |
| DN     | 368             | 6.0        | 339 (711)  | 12.61 | (13.00)             | 0.40  | (0.50)  | 220 (320)     | 550 | (690) | 0.50 (0.65) |
| KS     | 80%             | 98%        | 85%        | 97%   | 99%                 | 70%   |         |               |     |        |           |

The columns are as in Table 1. The last line shows the significance levels of the difference of the distributions, by the Kolmogorov-Smirnov test.

Observations show that groups and clusters of galaxies in high density regions, in the vicinity of rich clusters of galaxies and in superclusters, are more massive and luminous and have larger velocity dispersions than loose groups in average (Einasto et al. 2003a, 2003b, 2003c, 2003d, 2004a, 2004b). This enhancement extends to scales up to about $15-20 h^{-1}$ Mpc around rich clusters.

Ragone et al. (2004) determined groups of galaxies for the 2dF Galaxy Redshift Survey and studied the properties of these groups in the vicinity of rich clusters. This study confirms the results obtained in Einasto et al. (2003b): groups in the vicinity of rich clusters of galaxies are themselves also richer and more massive than groups in average.

In Einasto et al. (2003c) we studied the environmental enhancement of the LCLGs in superclusters. In particular, we calculated for the LCLGs in superclusters the distance to the nearest Abell cluster in supercluster and studied the properties of the LCLGs as a function of the distance to the nearest rich cluster in supercluster. In analogy to that test we plot the distribution of rms velocities of low mass haloes in the vicinity of the massive haloes (Fig. 7, right panel). Note the similarity of Fig. 7 right panel, and Fig. 5 in Einasto et al. (2003d): groups close to rich clusters have larger rms velocities than groups far from rich clusters in a supercluster.

Several studies of the correlation function of nearby groups of galaxies show that groups of higher mass are more strongly
clustered than groups on average (Giuricin et al. 2001, Girardi et al. 2000, and Merchan et al. 2000). Stronger clustering is an indication that these groups could be located in high density regions (Einasto et al. 1997).

Plionis, Basilakos and Tovmassian (2004) showed that the shapes of poor groups of galaxies depend on their richness, poorer groups being more elongated than richer groups and clusters of galaxies. Observations show that very rich clusters of galaxies also are elongated (see references in Plionis, Basilakos and Tovmassian 2004). This is in accordance with our results, showing that the poorest haloes have larger eccentricities than haloes of medium richness, and the most rich haloes again have larger eccentricities than medium rich haloes.

Several studies of clusters of galaxies have provided evidence that properties of rich clusters depend on their large scale environment (Novikov et al. 1999, Chambers et al. 2002, Einasto et al. 2001, Schuecker et al. 2001 and Plionis and Basilakos 2002) up to a distance of about 20 $h^{-1}$ Mpc. This distance is close to the so-called “pancake scale” (Melott & Shandarin 1993), and corresponds to the mean thickness of superclusters (Einasto et al. 1997 and Jaaniste et al. 1998).

Our results about the properties of haloes in different environments are in accordance with these observational results. The LCDM model haloes in high density regions are richer, more massive etc than haloes in low density environment. In particular, low mass haloes around the most massive haloes are themselves also more massive and have larger velocities than haloes farther away from massive haloes.

Our study shows that haloes move toward massive systems. In the vicinity of massive systems the velocities of haloes are larger than in low density regions (voids). This is in accordance with observational studies of velocity fields of galaxy clusters which show that clusters are moving toward superclusters of galaxies (Hudson et al. 2004 and references therein).

5.2. Comparison with simulations

Ragone et al. (2004) determined groups of galaxies from simulations by the Virgo Consortium, and studied the properties of these groups in the vicinity of rich clusters. This study confirmed the results obtained using observational data: groups in the vicinity of rich clusters of galaxies are themselves also richer and more massive than groups in average.

Ragone et al. (2004) also found that the enhancement of the properties of low mass haloes in the vicinity of massive haloes is a strong function of the mass of these massive haloes, while we did not detect such a strong dependence (except for 3D velocities). This difference is probably due to the fact that in this test, Ragone et al. (2004) used different host samples with increasing mass limit for host haloes, while we did not change the host sample.

Suhtonenko (2003) has demonstrated using different N-body simulations that in simulated superclusters more massive clusters are located in the central regions of superclusters. Gottlöber et al. (2002) and Faltenbacher et al. (2002) analysed high-resolution simulations of formation of galaxies, groups, and clusters, and found a significant enhancement of the mass of haloes in the environment of other haloes. This effect is especially significant at scales below 10 $h^{-1}$ Mpc. Therefore, environmental enhancement of the halo mass is a direct evidence for the process of the hierarchical formation of galaxy and cluster haloes. Halos inside clusters formed earlier than haloes in low density filaments and are more evolved (Gottlöber, Klypin and Kravtsov 2001, Gottlöber et al. 2003).

Kasun and Evrard (2003) found that the shapes of LCDM haloes do not depend on the large scale (supercluster) environment of haloes. However, the small hint of the such correlation seen in our study may ensue from the different definitions of the environmental density.

The finding that the richest haloes have larger eccentricities is in accordance with the recent results by Hopkins, Bahcall and Bode (2004) who also found that clusters are aligned with one another, in accordance with several observational studies (see references therein).
We studied the properties of dark matter haloes in different environments. Our main results are as follows.

- We composed a catalogue of haloes found using the MLAPM code and the FoF algorithm with a linking length of 0.23 in the units of mean particle separation. This catalogue is available from our web pages.

- Our analysis shows that haloes in high density environments, in general, are richer, more massive and have larger velocity dispersions than haloes in low density environment.

- Low mass haloes in the vicinity of high mass haloes are themselves richer, more massive, slightly more spherical and have larger rms velocity dispersions than low mass haloes farther away from high mass haloes. The larger the mass of parent halo, the larger are the velocities of low mass haloes in the vicinity of high mass haloes.

- Our study indicates the importance of the role of a high density environment, which affects the properties (formation and evolution) of galaxy systems. In high density regions haloes formed earlier, and are more evolved than haloes in low density regions, in accordance with the scenario of the hierarchical formation of the structure in the Universe.

6. Conclusions

We studied the properties of dark matter haloes in different environments. Our main results are as follows.

- We composed a catalogue of haloes found using the MLAPM code and the FoF algorithm with a linking length of 0.23 in the units of mean particle separation. This catalogue is available from our web pages.

- Our analysis shows that haloes in a high density environment are richer, more massive, have larger virial radii, have larger rms velocities, have larger peculiar velocities and are more spherical than haloes in a low density environment.
