Spectroscopic properties and energy transfer parameters of Er$^{3+}$-doped fluorozirconate and oxyfluoroaluminate glasses

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Er$^{3+}$-doped fluorozirconate (ZrF$_4$-BaF$_2$-YF$_3$-AlF$_3$) and oxyfluoroaluminate glasses are successfully prepared here. These glasses exhibit significant superiority compared with traditional fluorozirconate glass (ZrF$_4$-BaF$_2$-LaF$_3$-AlF$_3$-NaF) because of their higher temperature of glass transition and better resistance to water corrosion. Judd-Ofelt (J-O) intensity parameters are evaluated and used to compute the radiative properties based on the VIS-NIR absorption spectra. Broad emission bands located at 1535 and 2708 nm are observed, and large calculated emission sections are obtained. The intensity of 2708 nm emission closely relates to the phonon energy of host glass. A lower phonon energy leads to a more intensive 2708 nm emission. The energy transfer processes of Er$^{3+}$ ions are discussed and lifetime of Er$^{3+}$: 4I$_{13/2}$ is measured. It is the first time to observe that a longer lifetime of the 4I$_{13/2}$ level leads to a less intensive 1535 nm emission, because the lifetime is long enough to generate excited state absorption (ESA) and energy transfer (ET) processes. These results indicate that the novel glasses possess better chemical and thermal properties as well as excellent optical properties compared with ZBLAN glass. These Er$^{3+}$-doped ZBYA and oxyfluoroaluminate glasses have potential applications as laser materials.

Rare-earth elements are of interest in several high-tech and environmental applications$^{1-6}$. Over the past decades, Er$^{3+}$ has become one of the most interesting centers of research because of its 1.55 and 2.7 $\mu$m emissions from 4I$_{15/2}$ $\rightarrow$ 4I$_{13/2}$ and 4I$_{11/2}$ $\rightarrow$ 4I$_{13/2}$ transitions, respectively$^{4,7-11}$. The Er$^{3+}$-doped fiber amplifier is one of the important devices used in the 1.5 $\mu$m wavelength optical communication window. Er$^{3+}$ waveguide laser and up-conversion laser operations have been achieved at room temperature$^{12}$. The optical properties of Er$^{3+}$ are interesting because of their applications in infrared lasers operating at eye-safe wavelengths$^{8,13}$. 2.7 $\mu$m emission is also becoming a concern for researchers owing to the strong absorption of radiation by water. It has potential applications in medicine, sensing, and military countermeasures, as well as in light detection and ranging$^{14,15}$. Meanwhile, the maturity of laser diodes (LDS) accelerates Er$^{3+}$ development because of its efficient absorption at 800 or 980 nm.

Glasses known as convenient hosts for rare earth ions have been widely used because of their good mechanical and thermal stability, low synthesis cost, as well as possibility of pulling to fiber$^{16}$. Er$^{3+}$-doped fluoride, chalcogenide, silicate, and heavy metal oxide (tellurite, germanate, and bismuthate) glasses have been investigated for applications in near- and mid-infrared (IR) regions$^{4,17}$. Fluoride glasses are potential candidates for Er$^{3+}$ doped materials because of their low phonon energy and wide optical transmission window, ranging from UV to mid-IR$^{8,19}$. The fluorozirconate system, notably the ZrF$_4$-BaF$_2$-LaF$_3$-AlF$_3$-NaF (ZBLAN) glass composition, is one of the most stable systems against devitrification among fluoride glasses. However, Er$^{3+}$: ZBLAN fiber lasers have poor thermal properties (i.e., very low melting temperatures and high heat generation of Er$^{3+}$ actives ions) compared with those of near-IR silica-based fiber lasers, and the relatively large loss of ZBLAN fibers limits the usable length of the fibers, so further scaling up the power output is fundamentally difficult$^{20,21}$. Thus, exploring effective fluoride glasses for host matrices becomes a challenge to researchers, for example the fluorozirconate system (ZBYA)$^{22}$.

Fluoroaluminate glasses (AlF$_3$-based glasses) have better chemical durability and enhanced mechanical strength than fluorozirconate glasses, which would thus be useful for optical applications$^{23}$. However, some
devitrification problems are associated with these glasses. The addition of some oxides, especially Al(PO₃)₃ or TeO₂, is effective to stabilize the glass state. Oxfluoroaluminate glasses containing low P or Te have potential applications as hosts for high-power glass lasers.

Several structural studies have revealed the basic structure of these glasses (ZBYA and oxfluoroaluminate glasses). However, few investigations are available on the thermal, chemical, and the 1.5 and 2.7 μm emissions properties of these Er⁺⁺⁺ doped glasses. In this study, fluorozirconate glass (ZBYA) and oxfluoroaluminate glasses containing low P or Te are successfully prepared. The thermal and chemical properties of these glasses are investigated. The absorption and emission spectra at near- and mid-IR regions are tested. Simultaneously, the spectroscopic properties, Judd-Ofelt theory analysis results, cross sections, and emission parameters of these glasses are discussed.

### Experimental

The compositions of the glasses were ZrF₄-BaF₂-YF₃-AlF₃-1ErF₃ (designated as ZBYA), 99(AlF₃-YF₃-CaF₂-BaF₂-SrF₂-MgF₂)–1Al(PO₃)₃–1ErF₃ (designated as AYFP or FP) and 90(AlF₃-YF₃-CaF₂-BaF₂-SrF₂-MgF₂)–10TeO₂–1ErF₃ (designated as AYFT or FT). For comparison, fluorozirconate glass with composition of 100(ZrF₄-BaF₂-LaF₃-AlF₃-NaF)–1ErF₃ (designated as ZBLAN) was prepared. The samples were prepared using high-purity ZrF₄, AlF₃, YF₃, CaF₂, BaF₂, SrF₂, MgF₂, Al(PO₃)₃, TeO₂ and ErF₃ powders. Well-mixed 25 g batches of the samples were placed in platinum crucibles and melted at about 1100°C for 30 min. Then the melts were poured onto a preheated copper mold and annealed in a furnace around the glass transition temperature. The annealed samples were fabricated and polished to the size of 20 mm × 15 mm × 1 mm for the optical property measurements.

The characteristic temperatures (temperature of glass transition Tg and temperature of onset crystallization peak Tc) of the samples were determined using a NetzschSTA449/C differential scanning calorimetry at a heating rate of 10 K/min. The densities and refractive indices of the samples were measured through the Archimedes method using distilled water as an immersion liquid and the prism minimum deviation method respectively. Furthermore, the absorption spectra were recorded with a Perkin-Elmer Lambda 900 UV/VIS/NIR spectrophotometer in the range of 300 nm to 1600 nm, and the emission spectra were measured with a Triax 320 type spectrometer (Jobin-Yvon Co., France). All the measurements were carried out at room temperature.

### Results and discussion

#### Differential scanning calorimeter results

Fig. 1 shows the DSC results of the four samples in this study. Characteristic temperatures of Tg (temperature of glass transition), Tc (temperature of onset of crystallization), and Tp (temperature of peak of crystallization) are also marked in Fig. 1. Tg is an important factor for laser glass, higher values of the oxfluoroaluminate glasses compared with those of fluorozirconate glasses and other reported glasses give glass good thermal stability to resist thermal damage at high pumping intensities. The glass criterion, ΔT = Tc – Tg introduced by Dietzel, is often regarded as an important parameter for evaluating the glass forming ability. ΔT has been frequently used as a rough criterion to measure glass thermal stability. A large ΔT indicates strong inhibition of nucleation and crystallization. The glass formation factor of the materials is given by the parameter k is defined as (Tk – Tc)/(Tm – Tc), where Tm is the melting temperature of the glass. Compared with ΔT, the parameter is more suitable in estimating the glass thermal stability. A larger k indicates better forming ability of the glass. The glass forming ability can be estimated by these given characteristic temperatures. The existing stability criterion parameters ΔT and kare shown in Table 1. These values are larger than those of fluoride and phosphate glasses. These results indicate that the ZBYA and oxfluoroaluminate glasses have better forming ability and thermal stability against crystallization.

#### Chemical stability

The chemical durability of the sample was measured as follows: First, the weighed sample (W1) was placed into the distilled water. Second, the sample was kept in a thermostatic water bath at 98°C for 1 h and then cooled and dried in a drying box at 70°C for 1 h. Finally, the dry sample was weighed again (W2). The chemical durability of glasses was evaluated using the value of ΔW% = (W1 – W2)/W1 × 100%. The boiled water treatment process was repeated five times for each sample in this research. The results of the ΔW% are shown in Table 1. ZBLAN exhibits poorer resistance to water corrosion compared with the other samples, which coincides with the reported phenomenon.

The transmittance spectra of the samples before and after water treatment are shown in Fig. 2. Figure 2(a) shows the transmittance spectra of the samples without any treatment. Transmittance can reach as high as 90%, whereas approximately 10% loss contains the Fresnel reflection dispersion, and glass absorption. The fluorozirconate glasses have a weak absorption band at about 4500 nm because...
of CO₂ absorption, and the oxyfluoroaluminate glasses possess an absorption band at about 4750 nm because of the vibration peak [XO]. However, these fluctuations do not influence the near- and mid-infrared emissions of Er³⁺. The phonon energy can be inferred from the transmittance spectra, and large phonon energy increases the nonradiative decay rate. A higher nonradiative decay rate results in fewer radiative transitions and therefore less intense fluorescence bands. The phonon energy calculated by this model is also presented in Figure 2 (a). ZBYA glass has the smallest phonon energy and the IR cut-off wavelength is at about 7 μm.

The transmittance spectra of the samples after water treatment are shown in Figures 2(b) and 2(c). The basic form of the spectra almost remains the same for ZBYA, FP, and FT samples. Only the absorption band at about 2900 nm caused by OH²⁻ obviously changes. The OH⁻ in glass is related to the emission efficiency of rare-earth ions, because the residual OH⁻ groups will participate in the energy transfer of rare-earth ions and reduce the intensity of emissions. The OH⁻ group content in the glass can be expressed by the absorption coefficient of the OH⁻ vibration band at 3 μm, which can be given by

$$\alpha_{OH^-} = \frac{\ln (T/T_0)}{l}$$

where l is the thickness of the sample, T₀ and T are the transmitted and incident intensities respectively. Figures 2(c) describes the relationship between the OH⁻ absorption coefficient and the time of water treatment for ZBYA, FP, and FT samples. The OH⁻ absorption coefficients of the original samples are 0.055, 0.060, and 0.096 cm⁻¹, respectively, which are significantly lower than some reported values of bismuthate glass, germanate glass, and fluorophosphates glass. Some lower OH⁻ content glasses have also been reported recently and it is reported that the OH⁻ absorption coefficient should be < 2 cm⁻¹ to achieve optimum laser performance. The values of the present glasses are far less than 2 cm⁻¹. Therefore, excellent transmission property provides these Er³⁺-doped glasses with potential applications as laser materials. The OH⁻ absorption coefficient becomes larger for all the samples with increasing water treatment time, and ZBYA glass possesses best chemical stability according to Fig. 2(c). The ZBLAN sample has poor resistance to water corrosion. The spectra for the ZBLAN sample after water treatment are demonstrated alone in Fig. 2(b). After 1 h water treatment, the transmittance noticeably declines and the OH⁻ absorption coefficient approaches near infinity. Afterward, the ZBLAN glass becomes opaque at the mid-IR region.

Absorption spectra and calculation of optical parameters. Fig. 3 indicates the absorption spectra of the samples at room temperature in the wavelength region of 300 nm to 1600 nm. Absorption bands corresponding to the transitions starting from the ⁴I₁₅/₂ ground state to the higher levels ⁴I₁₃/₂, ⁴I₁₁/₂, ⁴I₉/₂, ⁴F₉/₂, ⁴F₇/₂, ⁴H₁₁/₂, and ⁴F₇/₂ are labeled. The shape and peak positions of each transition for the Er³⁺-doped glasses are very similar to those of other Er³⁺-doped glasses, indicating homogeneous incorporation of the Er³⁺ ions in the glassy network without clustering and changes in the local ligand field. The
absorption band around 980 nm indicates that these glasses can be efficiently excited by 980 nm LD.

Important spectroscopic and laser parameters of rare earth doped glasses have been commonly analyzed using the Judd–Ofelt theory. Details of the theory and method have been well described earlier, so only the results will be presented in this section. The intensity parameters of these Er3+-doped glasses are calculated and shown in the Table 2. The room-mean-square error deviation of intensity parameters is 3.10^-2, which indicates the validity of the Judd-Ofelt theory for predicting the spectral intensities of Er3+ and the reliability of the calculations. Previous studies have revealed that V2 parameters are indicative of the amount of the covalent bond, and are strongly dependent on the local environment of the ion sites, whereas the V6 parameter is related to the overlap integrals of the 4f and 5d orbits. Values of V4 and V6 also provide some information on the rigidity and viscosity of the hosts. However, compared with V2, which bears higher sensitivity to the chemical nature of the hosts, structural information carried by V4 and V6 values is marginal and sometimes inaccurate. An analysis of the values of V2 shows that the FP sample possesses lower covalence and higher symmetry. Compared with oxide glasses, fluoride glasses have smaller V2 because an F2- ion possesses higher polarizability than an O2- ion.

The calculated predicted spontaneous transition probability (A), branching ratio (β) and radiative lifetime (τrad) of certain optical transitions for Er3+-doped fluoride glasses are also shown in Table 2. The predicted spontaneous emission probabilities of Er3+ transitions are much higher than reported values. Higher spontaneous emission probability provides a better opportunity to obtain laser actions.

**Fluorescence properties and energy transfer processes.** Under 980 nm diode laser excitation, the 4I13/2 → 4I5/2 fluorescence around 1.5 μm and 4I11/2 → 4I5/2 fluorescence around 2.7 μm are obviously observed, as seen in Fig. 4. For the present samples, no shift in the wavelength of the emission peaks is observed, but the peak intensity is evidently different. Generally, the intensity of 1530 nm is opposite of that of 2710 nm for the same sample in this study. The fluorozirconate glasses possess more intensive 2708 nm emission owing to the lower phonon energy. The multi-phonon nonradiative decay rate is given by the well-known energy gap law:

\[ W_n = W_0 \left(1 - e^{-\left(\frac{hv}{kT}\right)}\right) \]

where \( W_n \) is the rate at temperature T, \( W_0 \) is the rate at 0 K, n = ΔE/ hv, ΔE is the energy gap between the levels involved, v is the relevant phonon frequency.

**Figure 3 | Absorption spectra of the present samples.**
phonon’s frequency. When $\Delta E$ is equal to or less than 4–5 times the high-energy phonons, the multi-phonon nonradiative relaxation with the emission of a few high-energy phonons becomes competitive with radiative processes. The energy gap between the $^1I_{15/2}$ and $^1I_{13/2}$ levels is about 3690 cm$^{-1}$, which is equal to 5–6 times the high-energy phonons of the oxyfluoroaluminate glasses and 6–7 times that of the fluorozirconate glasses. The multi-phonon nonradiative relaxation with the 2.7 µm emission of the oxyfluoroaluminate glasses has a larger probability than that of the fluorozirconate glasses, which leads to a much lower intensity of the 2.7 µm emission. The higher intensity of the 1.5 µm emission of the oxyfluoroaluminate glasses can be explained by the $^1I_{13/2}$ level decay lifetime of the samples, which will be discussed below.

The upconversion spectra of the present samples are shown in Fig. 5(a). In this region, the green emissions at about 545 and 550 nm dominate. The green emission of the fluorozirconate glasses is stronger than that of the oxyfluoroaluminate glasses, which is similar to the emission of 2710 nm and opposite to that of the 1530 nm emission. To explain the relationship among the green emission, and the near- and mid-IR emissions, the energy level of $\text{Er}^{3+}$ is demonstrated in Fig. 5(b). Ions of the $^1I_{15/2}$ state are excited to the $^1I_{11/2}$ state by ground state absorption (GSA) when the prepared samples are pumped by a 980 nm LD. On the one hand, some ions in the $^1I_{11/2}$ level undergo the energy transfer upconversion (ETU1) and excited stated absorption (ESA1) processes, thus contributing to the population of $^4F_{7/2}$ level. Afterward, the excited energy stored in the...
\(^{4}F_{9/2}\) level decays nonradiatively to the next- lower \(^{2}H_{11/2}\) and \(^{4}S_{3/2}\) levels. The green emission can be attributed to the Er\(^{3+}:^{4}H_{11/2} \rightarrow ^{4}I_{15/2}\) and \(^{4}S_{3/2} \rightarrow ^{4}I_{15/2}\) transitions. Some may have the chance to decrease to the lower \(^{4}F_{9/2}\) energy through nonradiative decay, after which red emission (Er\(^{3+}:^{2}F_{9/2} \rightarrow ^{4}I_{15/2}\)) occurs. On the other hand, ions in the \(^{4}I_{11/2}\) level decay radiatively to the \(^{4}I_{13/2}\) with 2.7 \(\mu\)m emission or nonradiatively to the \(^{4}I_{13/2}\) level. Then the 1.5 \(\mu\)m emission occurs because of the \(^{4}I_{13/2} \rightarrow ^{4}I_{15/2}\) transition.

Fig. 6 shows the experimental decays of the Er\(^{3+}:^{4}I_{13/2}\) level at room temperature of the present samples. The lifetime is an important factor for potential laser materials. All the samples show an exponential decay with lifetime of 10.09, 6.66, 4.91, and 4.06 ms, respectively, which are larger than those of tellurite glass (3.3 ms)\(^{42}\), bismuth based glass (1.8 ms)\(^{42}\), and borosilicate glass (2.0 ms)\(^{43}\). Difference exists between the values of lifetime that are measured and calculated because the measurement occurs at room temperature, but not at low temperature. The measured lifetimes of the fluorozirconate glasses are longer than those calculated ones owing to the serious self-absorption of the \(^{4}I_{13/2}\) level. The fluorozirconate glasses possess longer lifetime of Er\(^{3+}:^{4}I_{13/2}\) level but smaller intensity of 1.5 \(\mu\)m emission or nonradiatively to the \(^{4}I_{13/2}\) level. Then the 1.5 \(\mu\)m emission occurs because of the \(^{4}I_{13/2} \rightarrow ^{4}I_{15/2}\) transition.

Cross sections and emission parameters. Beer-Lambert\(^{44}\) and Fuchtbauer-Ladenburg\(^{45}\) equations are commonly used to calculate the cross section. The difference is that the former calculates the absorption cross section based on the absorption spectra firstly, whereas the latter calculates the emission cross section primarily based on the emission spectra and spontaneous transition probability. Both relate the absorption and emission cross sections through McCumber theory\(^{36}\). The equations are as follows:

**Beer—Lambert equation:**
\[
\sigma_a(\lambda) = \frac{2.303\log(I_0/I)}{Nl}
\]

where \(\log(I_0/I)\) is the absorbance from absorption spectrum, \(I\) is the thickness of the glass and \(N\) is the ion density.

**Fuchtbauer—Ladenburg equation:**
\[
\sigma_e = \frac{\lambda^2 A_{rad}}{8\pi c n^2} \frac{\lambda I(\lambda)}{\int \lambda I(\lambda) d\lambda}
\]

where \(\lambda\) is the wavelength, \(A_{rad}\) is the spontaneous transition probability, \(I(\lambda)\) is the emission spectrum, and \(n\) and \(c\) are the refractive index and light speed in vacuum respectively.

**McCumber equation:**
\[
\sigma_e(\lambda) = \sigma_a(\lambda) \left[ \frac{Z_u}{Z_d} \right] e^{\left(\frac{2n\lambda k_B T}{h}\right)}
\]

where \(h\) is Planck’s constant, \(k_B\) is the Boltzmann constant, \(T\) is the temperature, \(E_d\) is the ground state manifold and the lowest stark level of the upper manifolds and \(Z_u\) and \(Z_d\) are partition functions of the lower and upper manifolds.

The absorption and emission cross sections of 1.5 \(\mu\)m for all present glasses are calculated using both methods. The results are shown in Table 3. The values calculated using BL method are larger than...
those obtained using FL equation. Nevertheless, the same trend emerges, namely, the value of the absorption cross section is somewhat smaller than that of the emission cross section and the fluorozirconate glasses possess larger values compared with oxyfluoroaluminate glasses. To demonstrate the difference between the values calculated by the two equations, the cross sections at about 1.5 μm are described in Fig. 7 for the FP samples (similar spectra of other samples). The curves calculated from the FL equation seem smoother. FL may be more theoretically accurate because it is based on both the emission and the absorption spectra (the calculated spontaneous transition probability is based on the absorption spectra).

Full width at half maximum (FWHM) is a determiner for 1.5 μm laser materials. The larger bandwidth of this transition is suitable for tunable lasers delivering relatively constant power over a wide wavelength range. The 1.5 μm emission from Er3+-doped silicate glasses extensively used in the present study exhibit a narrow FWHM of about 30 nm, which limits their further applications. The effective line width (Δλ_eff) is reportedly more accurate in estimating the bandwidth of this transition than FWHM because the emission band is slightly asymmetric. The effective line width (Δλ_eff) is determined using the expression:

\[ \Delta \lambda_{\text{eff}} = \int \frac{I(\lambda) d\lambda}{I_{\text{max}}} \]

where \( I_{\text{max}} \) is the peak fluorescence intensity corresponding to \( \lambda_{\text{eff}} \) (the peak fluorescence wavelength). The \( \Delta \lambda_{\text{eff}} \) values of 1.5 μm emission are presented in Table 3. The effective line width values in the present glasses are higher than those of silicate (34.8 nm) and phosphate (46.0 nm), making these fluoride glasses promising candidates for broadband amplifiers in WDM systems.

As known, a figure of merit (FOM) for the amplifier bandwidth is the product FWHM × σ_em^0, which can be inferred from Table 3. The products of the samples are much higher than those of ZBLAN (30 pm^2·nm) and Al/SiO2 (25 pm^2·nm) glasses, which have been studied as potential EDFA hosts. Meanwhile, the FOM for amplifier gain is usually defined as the product of stimulated emission cross section and lifetime (σ_em × τ_exp). As far as the material aspects are concerned, a larger product of σ_em × τ_exp is desirable for an efficient fiber amplifier. The product of ZBYA glass has an obvious advantage over Al/SiO2 (5.5 pm^2·ms). These results show that Er3+-doped fluoride glasses are promising candidate materials for 1.5 μm signal amplification.

Based on Fig. 4(b) and Eqn (3) to (6), the emission cross section and the effective line width of Er3+:2.7 μm are calculated, as shown in Table 3. The maximum emission cross section occurs at 2708 nm, and the values are above 7 × 10⁻²¹ cm² for all samples, which are higher than the reported values of 0.45 × 10⁻²⁰ cm² in the YAG crystal, 0.53 × 10⁻²⁰ cm² in the LiYF₄ crystal, 0.54 × 10⁻²⁰ cm² in the ZBLAN glass, and 0.66 × 10⁻²⁰ cm² in the chalcophosphate glass.

**Table 3 | Calculated emission and absorption cross section and effective line width around 1.5 and 2.7 μm of the present glasses obtained through both BL and FL equations**

| Glass  | σ_em(BL) (×10⁻²⁰ cm²) | σ_abs(BL) (×10⁻²⁰ cm²) | σ_em(FL) (×10⁻²¹ cm²) | σ_abs(FL) (×10⁻²¹ cm²) | Δλ [nm] | τ_exp [ms] |
|--------|------------------------|-------------------------|------------------------|------------------------|---------|------------|
| ZBYA   | 6.79                   | 8.95                    | 4.55                   | 6.29                   | 75.6    | 6.82       |
| ZBLAN  | 5.79                   | 7.26                    | 4.84                   | 6.56                   | 77.3    | 6.44       |
| FP     | 5.26                   | 6.61                    | 3.01                   | 4.18                   | 77.3    | 11.17      |
| FT     | 5.23                   | 6.98                    | 4.01                   | 5.56                   | 73.6    | 8.15       |

**Figure 7 | The calculated emission and absorption cross section spectra around 1.5 μm emission of FP glass through both BL and FL equations.**
where $C_{DA}$ is the energy transfer coefficient, $R$ is the distance of separation between donor and acceptor, and the critical radius of the interaction can be obtained using the equation $R_c = C_{D-A}^{-1/4}$, where $\tau_p$ is the intracenter lifetime of the excited level of donor. The expression for direct transfer (D-A) is then expressed by:

$$C_{DA} = \frac{6\alpha_0}{(2\pi)^2 n^2 \mu^2} \sum_{m=0}^{\infty} \sum_{n=0}^{\infty} \frac{m!}{(m+n)!} \left(\frac{\sigma^{DA}_{m,n}}{\lambda}\right)^2 e^{-2R_c}$$

(10)

Energy transfer properties of $4I_{13/2}$ level in the present glasses are calculated using Eqs. (7) to (10) and are listed in Table 4. The number of phonons necessary to assist the energy transfer process is also indicated along with its contribution (%).

### Table 4 | Calculated interaction microscopic parameters $C_{D-A}$ for $4I_{13/2}$ level in the present glasses. The number # of phonons necessary to assist the energy transfer process is also indicated along with its contribution (%).

| Glass | N (No. of phonons) [%] | Phonon assisted | Transfer coefficient ($10^{-39}$ cm$^3$/s) |
|-------|------------------------|----------------|-----------------------------------------|
| ZBYA  | 0                      | 1              | 3.99                                    |
| ZBLAN | 0                      | 1              | 4.53                                    |
| FP    | 3.0%                   | 0              | 1.94                                    |
| FT    | 0.2%                   | 0              | 2.95                                    |

In conclusion, Er$^{3+}$ ions are calculated. Therefore, the Er$^{3+}$ ions are an efficient near- and mid-infrared emission source. The energy transfer process is dominated by the donor-acceptor mechanism, which will be promising materials for infrared lasers and optical amplifiers.

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Additional information
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