Colour gradients within SDSS DR7 galaxies: hints of recent evolution

V. Gonzalez-Perez,1,2* F. J. Castander2 and G. Kauffmann3

1Institute for Computational Cosmology, Department of Physics, University of Durham, South Road, Durham DH1 3LE
2Institut de Ciències de l’Espai (CSIC/IEEC), F. de Ciències, Torre C5 Par 2a, UAB, Bellaterra, 08193 Barcelona, Spain
3Max-Planck Institut für Astrophysik, D-85741 Garching, Germany

Accepted 2010 September 21. Received 2010 September 21; in original form 2010 June 2

ABSTRACT
The evolutionary path followed by a galaxy shapes its internal structure, and, in particular, its internal colour variation. We present a study of the internal colour variation within galaxies from the Seventh Data Release of the Sloan Digital Sky Survey (SDSS DR7). We statistically study the connection between the internal colour variation and global galactic properties, looking for hints of the recent galactic evolution. Considering only galaxies with good photometry and spectral measurements, we define four luminosity-threshold samples within the redshift range $0.01 < z < 0.17$, each containing more than 48 000 galaxies. Colour gradients are calculated for these galaxies from the surface brightness measurements provided by the SDSS DR7. Possible systematic effects in their determination have been analysed. We find that, on average, galaxies have redder cores than their external parts. We also find that it is more likely to find steep colour gradients among late-type galaxies. This result holds for a range of classifications based on both morphological and spectral characteristics. In fact, our results relate, on average, steep colour gradients to a higher presence of young stars within a galaxy. Our results also suggest that nuclear activity is a marginal driver for creating steep colour gradients in massive galaxies. We have selected pairs of interacting galaxies, with a separation of 5 arcsec, in projected radius, and a difference in redshift of 100 km s$^{-1}$, finding that they present steeper gradients than the average population, skewed towards bluer cores [Correction added after online publication 2010 November 22: arcmin changed to arcsec]. Our analysis implies that colour gradients can be useful for selecting galaxies that have suffered a recent (minor) burst of star formation.

Key words: galaxies: fundamental parameters – galaxies: statistics – galaxies: structure.

1 INTRODUCTION
The subtleties of galaxy formation remain to be understood. The study of the internal structure of galaxies can help us to understand how they formed and evolved. Here we study the internal colour variation across galaxies, quantified through their colour gradient. Interest in internal colour variation has grown enormously in the last five years, especially due to the availability of both shallow and deep surveys such as the Sloan Digital Sky Survey (SDSS; York et al. 2000), that can provide statistically significant samples of galaxies, and deep surveys, that provide high-resolution images of galaxies at $z > 0.5$, such as those performed with the Hubble Space Telescope (HST; e.g. Menanteau et al. 2005; Ferreras et al. 2009). Previous work has used the colour gradient as a measure of the galactic internal colour variation, which has proved to be very useful for exploring galactic properties, due to its tight dependency on the galactic distribution of metallicity, stellar age and dust (see e.g. Michard 2005; Wu et al. 2005; Rawle, Smith & Lucey 2010; Tortora et al. 2010). This, together with the accessibility of gradient measurements, since only photometry is needed, makes the colour gradient a useful tool to obtain statistical results for wide samples of galaxies, that will be interesting to relate to different theoretical aspects from models of galaxy formation.

In general, galaxies tend to have cores that are redder than their external parts (e.g. Peletier et al. 1990). In this work we study the variation within nearby galaxies of the following optical colours: $(g - i), (g - r), (r - i), (i - z)$ and $(r - z)$. Both $(g - r)$ and $(g - i)$ rest frame colours are most sensitive to the intensity of the spectral break that appears around $4000$ Å, due to the accumulation of resonant absorption lines from metals in different stages of ionization (e.g. Hamilton 1985). This break correlates with the temperature of the dominant stellar population, increasing for cooler stars, but it does not depend strongly on the galactic metallicity. Unlike late-type galaxies, early-type ones are dominated by K-type stars, showing a rather steep change in flux from $g$ to $r$ or $i$ band. If we consider that these colours are mainly related to the age of the galaxy then the redder core will imply that it is also older.

*E-mail: violeta.gonzalez@durham.ac.uk
The other three colours, \((r - i), (r - z)\) and \((i - z)\), in the rest frame directly depend on the proportion of main sequence to red giant branch or older stars (Bruzual & Charlot 1993). Thus, we could simply record these colours as depending on the relative amount of old and young stars in the galaxies, though this is less clear for \((i - z)\) and has a smaller dynamic range in the case of the \((r - i)\) colour. Thus, we observe the same tendency as before: redder cores imply that in general galaxies tend to have older stars in their centres.

However, these implications should be taken with caution for two main reasons. (i) Global colours can be affected by marginal young populations (Li & Han 2007). (ii) Colours within different galactic annuli do not necessarily agree well with global ones. Besides, broad-band colours show a degeneracy in their dependence with stellar population age and metallicity (e.g. Worthey 1994; Charlot, Worthey & Bressan 1996). Indeed, several studies (see e.g. Tamura & Ohta 2004; Wu et al. 2005; La Barbera & de Carvalho 2009; Tortora et al. 2010) have shown that metallicity and not age gradients are the principal origin of the colour variation. In the case of early-type galaxies, age gradients have been measured to be almost flat or positive while metallicity gradients are negative, i.e. early-type galaxies tend to have younger, higher metallicity cores (see e.g. Sánchez-Blázquez, Gorgas & Cardiel 2006; Clemens et al. 2009; La Barbera & de Carvalho 2009; Rawle, Smith & Lucey 2010).

Late-type galaxies are more complex, showing a broad variety of age and also metallicity gradients, due to the interplay between dust content, stellar feedback, bursts of formation and stellar migration due to the instabilities that trigger the formation of bars but also the spiral arms. MacArthur, González & Courteau (2009) observed that spiral galaxies have bulges with positive age gradients, while their discs show negative ones, but there are examples of spiral galaxies with negative age gradients for most of their extension, except for the most external radii (Vlajić, Bland-Hawthorn & Freeman 2009).

Metallicity gradients within galaxies can be produced through different mechanisms. Winds generated by supernovae (Larson 1974) or active galactic nuclei (AGNs) (Begelman, de Kool & Sikora 1991) can provide the metallicity enrichment of the interstellar or even the inter galactic medium. Due to the multiple phases that compose this medium the enrichment does not necessarily happen in a symmetrical way, which can produce strong metallicity gradients and thus colour gradients. Galaxies with a significant age gradient can present very shallow or even inverted colour gradients (Hinckley & Im 2001), since age gradients usually arise from localized regions of star formation, generally resulting in galaxies with bluer cores than their external parts. The presence of a diffuse component of dust could also explain some colour gradients. However, this has a marginal impact, specially for early-type galaxies, which are almost dust free (Michard 2005; Wu et al. 2005). In summary, colour gradients in galaxies are likely to be related to the different star formation histories followed, which depend on the way gas is distributed and collapses after accretion and mergers.

Many studies of colour gradients try to clarify the dependence on the star formation history of galaxies. This aspect is of particular interest since it could help us to understand how galaxies form and evolve. The recent study by Suh et al. (2010) of early-type galaxies drawn from the SDSS DR6 reports a tight correlation between the existence of steep colour gradients and ongoing residual star formation. This study of galaxies at \(z < 0.06\) suggests a relation between elliptical galaxies with bluer cores presenting global bluer colours than average. Ferreras et al. (2009) found the same relation for spheroidal galaxies observed by the HST at 0.4 < \(z\) < 1.5. Lee et al. (2008) found that steeper colour gradients appear within star-forming galaxies, in both late and early types. A similar result was found in the recent study by Tortora et al. (2010), where older galaxies are observed to have systematically shallower age and metallicity gradients, and thus, colour gradients. The colour gradients of spiral galaxies appear to be dominated by the fact that, on average, their bulges are redder than their discs. However, this is an oversimplification for many late-type galaxies (see e.g. Bakos, Trujillo & Pohlen 2008).

Cosmological simulations do not yet have sufficient resolution to make predictions for colour gradients. However, semi-analytical models which include a bulge-disc decomposition and spatially resolved star formation, could provide some useful insight for this particular problem (Stringer & Benson 2007). Nevertheless, in general, gas-dynamical simulations with high enough resolution to follow physical processes within galaxies are needed in order to produce theoretical predictions for the internal characteristics of galaxies. ‘Monolithic collapse’ models can produce elliptical galaxies with colour gradients that agree with observations if a certain scatter is allowed for the star formation efficiency (Pipino et al. 2010). These monolithic models also predict steeper gradients for more massive galaxies, something that is observed up to \(M_* \sim 3.5 \times 10^{10} M_\odot\) (Spolaor et al. 2009; Rawle et al. 2010; Tortora et al. 2010). For more massive galaxies, the contribution of mergers provides a larger scatter that smears out such correlation. Kobayashi (2004) used chemo-dynamical simulations of merging galaxies to understand elliptical galaxy formation. The resultant galaxies had metallicity gradients consistent with observations. The predicted gradients depend strongly on the relative properties of the progenitor galaxies, i.e. on the particular formation process of a galaxy.

In this paper, we study the largest data set to date, which allows us to make a statistically robust analysis of the internal colour variation within nearby galaxies. We study four luminosity-threshold samples, defined in Section 2. We obtain colour gradients directly from the SDSS photometric data and we (K + e) correct global magnitudes using spectral energy distributions (SEDs) generated with PEGASE (Fioc & Rocca-Volmerange 1997). This process is described in Section 2.1. In Section 3 we analyse the colour gradients distribution and we also study the possible correlations between the colour gradient and global galactic properties, including galactic types and redshift. Finally we summarize our results and conclusions in Section 4.

In this study we use Petrosian magnitudes for setting the sample limits. Apparent magnitudes are corrected from the extinction due to our galaxy, but not to their internal reddening. Model magnitudes are used only for global galactic colours. All magnitudes used in this paper are in the AB system, unless otherwise specified. We assume a flat cosmology, \(\Omega_k = 0\), with a critical matter density of \(\Omega_m = 0.3\) and a Hubble constant, \(H_0 = 100 h \text{ km s}^{-1} \text{Mpc}^{-1}\) with \(h = 0.7\) (Spergel et. al. 2003).

2 THE DATA

Our sample is drawn from the SDSS DR7 (Abazajian et al. 2009) spectroscopic main galaxy targets. The SDSS DR7 has covered spectroscopically an area of \(9380 \text{ deg}^2\), providing a redshift accuracy of \(30 \text{ km s}^{-1}\) rms for the main galaxy sample. The SDSS main spectroscopic sample is described by Strauss et al. (2002). Galaxies within this sample have \(r < 17.77\) (Petrosian magnitude after correcting for galactic extinction) and a median redshift of \(\bar{z} \sim 0.1\).

From the SDSS main spectroscopic sample, we further select those galaxies that, according to the SDSS pipeline flags, have a
reliable determination of their redshift, a good photometry\textsuperscript{1} in all \(g\), \(r\), \(i\) and \(z\) bands, have a good determination of their Petrosian radius and a complete surface brightness profile measurement. In order to avoid those galaxies most affected by aperture effects, a lower limit to the galaxy redshift has been imposed, \(z > 0.01\).

After applying the above restrictions we found that one of the galaxies appeared multiple times due to different deblending of objects at successive scans. After taking out this galaxy our initial sample contains 339,711 galaxies.

As it will be detailed in Section 2.3 we quantify the internal colour variation using the SDSS DR7 measurements of surface brightness averaged within circular concentric annuli. At most there are 15 measurements, though, in most cases there are less due to the low surface brightness of many galaxies. The outer radii of these annuli are fixed and range from 0.22 to 258.38 arcsec, growing approximately exponentially.\textsuperscript{2}

We make use of the stellar masses, star formation rates, some spectral indices and classification provided in the SDSS MPA/JHU\textsuperscript{3} collaboration data base (Kauffmann et al. 2003a; Brinchmann et al. 2004), which has been updated for the SDSS DR7. These parameters are obtained by extrapolating to the full galaxy the spectroscopic information collected within the 3 arcsec diameter fibre set around the galactic centres. The extrapolation is done taking into account the global galactic colour and the effects due to dust. This extrapolation does not consider the colour gradients within galaxies, which could include a systematic effect on the determination of global properties.

2.1 (\(K+e\))-correction

The (\(K+e\))-correction accounts for two effects. One, the \(K\)-correction, is the shift of the filter in the galaxy’s rest frame with redshift due to observing with a fixed band (Oke & Sandage 1968). The other, the e-correction, accounts for the change in luminosity due to ageing of existing stellar populations or new star formation that galaxies experience up to a reference redshift, generally \(z = 0\) as in our case, from the epoch at which they are observed (Poggianti 1997). Both effects vary between the different bands. Within the SDSS bands we obtain larger corrections for bluer bands (Fukugita, Shimasaku & Ichikawa 1995). In order to make sure that we are comparing similar spectral regions from different galaxies we need to apply the (\(K+e\))-correction.

The (\(K+e\))-correction is evaluated fitting the galaxy photometry to the best model within a grid of SEDs generated with the population synthesis models PEGASE (Fioc & Rocca-Volmerange 1997). The grid is made using the default template SEDs produced within PEGASE, matching the colours observed for different Hubble galactic types at \(z = 0\), and includes a galaxy formed in a 1 Gyr long burst, an elliptical and a lenticular galaxies, spiral galaxies: Sa, Sb, Scb, Sc, Sd and three Irregular galaxies with different formation redshifts.

There are six galaxies in our initial sample with colours that are not well fitted by the synthetic ones. These are left out of the sample. Since these objects represent 0.002 per cent of the sample we do not apply any correction for their omission.

Both \(K\) and (\(K+e\)) corrections are shown in Fig. 1 for all galaxies in our initial sample. These corrections are applied to the global colours of galaxies in our sample. The (\(K\))-correction alone tends to be larger for higher redshifts, but the dispersion increases at the same time. This behaviour has been found in other works (see e.g. Blanton et al. 2003; Fukugita et al. 1995).

We can observe in Fig. 1 that the (\(K+e\))-correction shows a weaker dependency on redshift than the (\(K\))-correction. This was also found in previous studies, such as Poggianti (1997). The reason for this flattening is that as galaxies evolve, their luminosity decreases until a new burst of star formation occurs, being superimposed to an already old stellar population.

We checked the possibility of calculating the (\(K+e\))-correction individually for different galactic radii. For this purpose, we obtained magnitudes in circular concentric annuli for each galaxy, from the averaged surface brightness measured by the SDSS pipelines. However, colours in individual annuli are noisier than global ones and the fitting procedure basically fits noisy features that result in obtaining unrealistic SEDs for each annulus. Therefore, we obtain the global (\(K+e\))-correction for each galaxy, which presumably is an average of the correction to different annuli. The use of an average (\(K+e\))-correction could introduce spurious colour gradients. These are difficult to evaluate, since they depend on the intrinsic metallicity and age gradients of each galaxy, higher signal-to-noise ratio (S/N) data would be needed to properly compute these corrections as a function of radius and evaluate the effect of observing different radii at a given projected annulus. Applying a global correction implies that the resultant colour gradients would not be affected, since we are only moving the zero-point on the colour versus radius relation. This implies that similar colour gradients will be found either applying the (\(K+e\))-correction or only the (\(K\))-correction. However, applying one or the other changes very

\textsuperscript{1}By good photometry we mean here that according to the SDSS pipeline flags the galaxies are detected at more than 5\(\sigma\) level, with all their pixels checked for possible flux peaks, not being a blended object, without too many interpolated pixels, without pixels hit by a cosmic ray and without a faulty sky subtraction.

\textsuperscript{2}For further details we refer the reader to the SDSS help page http://cas.sdss.org/dr7/en/help/browser/constnants.asp?n=ProfileDefns and the document on profiles written by R. Lupton and J. Gunn: http://www.astro.princeton.edu/~rlf/photomisc/profiles.ps.

\textsuperscript{3}http://www.mpa-garching.mpg.de/SDSS/

© 2010 The Authors, MNRAS 411, 1151–1166
Monthly Notices of the Royal Astronomical Society © 2010 RAS
slightly the defined luminosity-threshold samples, and has a definite impact on the global colours associated to each galaxy.

We will restrict our study to galaxies seen up to such a redshift that the ($K + e$)-corrections would not be large. Rather than the actual value of the ($K + e$)-correction, the problem resides in the higher spread among template SEDs found at higher redshifts, which can introduce larger errors in the estimated correction. For the majority of galaxies up to $z < 0.17$, the ($K + e$)-corrections is well below a value of 0.6 in the $g$, $r$, $i$, and $z$ bands. For the same range, the $K$-correction stays below 0.8 in all bands. There is another reason for not considering galaxies at the highest redshifts covered by the survey. While the distribution of the $K$-correction is smooth, it is clear that our estimate of the ($K + e$)-correction start to be almost discretized for galaxies with $z \geq 0.25$. This effect is not present at $z < 0.17$. In order to correct galaxies at $z > 0.17$ we need to enhance our grid of model SEDs, including different formation redshifts for not only Irregular galaxies but also for all the Hubble types included as templates. This change should be done carefully, in order to reproduce the observed fluxes of galaxies at different evolutionary stages.

Taking into account the two mentioned sources of uncertainty we will restrict our study to galaxies with $z < 0.17$.

2.2 The luminosity-threshold samples

We have divided our initial sample of galaxies with $z < 0.17$ into four luminosity-threshold samples. These samples, though well defined, are not volume limited since they miss a cut in redshift corresponding to the bright limit of the survey. Fig. 2 shows the boundaries of each sample superimposed on the distribution of the absolute magnitude versus redshift for all galaxies. Absolute magnitudes have been obtained from the ($K + e$)-corrected Petrosian magnitudes in the $r$ band. Table 1 summarizes the characteristics of the luminosity-threshold samples. We will refer to each sample by their absolute magnitude cut, as indicated in the first column of Table 1.

We find that some of the galaxies within the S21 sample have a half light radius $R_{50} < 0.7$ arcsec, i.e. inside the first two annuli with surface brightness measurements. As explained in Section 2.3 these two annuli are not considered in the calculation of the colour gradients. Thus, for those galaxies within the S21 sample we will be calculating colour gradients with only the outer half of the galactic light. For this reason, we will concentrate on the other three samples at $z < 0.14$, and results from the S21 sample will be considered with caution.

As explained in the next Section 2.3, to obtain colour gradients, galaxies should have their surface brightness measured in at least four annuli, without considering the two innermost ones. Among our samples we find two galaxies which have their surface brightness measured in too few annuli, one within the sample S20.5 and the other within the S19 one. These two galaxies lack a colour gradient measurement and are not considered further.

As mentioned previously, we make use of some of the quantities derived from the SDSS data base by the MPA/JHU collaboration. The cross identification using the position coordinates of the galaxies is not perfect. Fewer than 5 per cent of the galaxies in our initial samples do not appear to have properties measured by the MPA/JHU collaboration. Only when using the MPA/JHU derived parameters we will be neglecting those galaxies.

2.3 Quantifying the internal colour variation through colour gradients

Different ways to compute the internal colour variation can be found in the literature. Some examples are: the slope of colour versus normalized radius or its logarithm (e.g. Hinkley & Im 2001; Michard 2005; Tortora et al. 2010), the difference between colours outside and inside certain radius (e.g. Menanteau et al. 2005; Park & Choi 2005), the comparison between model and fibre colours when working with galaxies from the SDSS (e.g. Roche, Bernardi & Hyde 2009) and the colour variation averaged to all the pixels in an image (e.g. Menanteau, Abraham & Ellis 2001).

In the early stages of this work we used the SDSS DR2 to estimate the best way to quantify the internal colour variation. We studied the internal colour variation within a sample of galaxies with a concentration index $C > 2.63$ and $z < 0.1$. The concentration index is defined as the ratio between two radii enclosing different amounts of light flux. The SDSS definition uses the radii containing 90 per cent, $R_{90}$, and 50 per cent, $R_{50}$, of the total galactic light. Strateva (2001) and Shimasaki (2001) found that $C = 2.6$ is the boundary that separates early from late-type galaxies, according to both their morphological and spectral features. The actual value of this boundary can vary depending on level of restriction needed for contaminants within one or the other type of galaxies.

After thoroughly testing various methods using the quantities provided by the SDSS data base, we reached the conclusion that the surface brightness profile appears to be the best way to quantify the internal colour variation in galaxies as opposed to magnitude based estimations, e.g. comparing the fibre or point spread function (PSF) colours with the global galactic colours.

Table 1. The given name, absolute magnitude range, redshift range and final number of galaxies to be studied within the defined luminosity-threshold samples.

| Name | Absolute magnitude | Redshift | No. of galaxies |
|------|--------------------|----------|-----------------|
| S19  | $M_r - 5 \log h < -19.$ | $0.01 < z < 0.072$ | 48 728 |
| S20  | $M_r - 5 \log h < -20.$ | $0.01 < z < 0.111$ | 82 838 |
| S20.5| $M_r - 5 \log h < -20.5$ | $0.01 < z < 0.1375$ | 86 818 |
| S21  | $M_r - 5 \log h < -21.$ | $0.01 < z < 0.169$ | 66 177 |

Figure 2. Redshift versus absolute magnitude in $r$ band for the selected SDSS DR7 galaxies. The different luminosity-threshold samples are enclosed by solid lines for the S19 sample, dashed for the S20, dotted for the S20.5 and dash–dotted for the S21.
The SDSS provides measurements of surface brightness averaged within circular concentric annuli at different galactic radii. We obtain colour gradients from these measurements. The two innermost annuli, \( R < 0.7 \) arcsec, are excluded from the calculation, since they are the most affected by seeing (the median PSF width in the \( r \) band for the SDSS DR7 is 1.4 arcsec). Previous studies, such as that from Tamura & Ohta (2003) have reported that the internal colour variation is diminished if the annuli most affected by seeing are considered for obtaining the surface brightness profile.

From the SDSS averaged surface brightness profile we get the cumulative one. This last one is fitted to a taut spline\(^4\), using a fourth order polynomial. Thus we need galaxies to have measurements of average surface brightness in at least four annuli. The interpolated surface brightness points are differentiated. We then convert the resulting surface brightness into magnitudes. We do this last step only for the radii corresponding to the outer ones from the initial annuli. These magnitudes are corrected with the global (\( K + e \))-correction obtained for the whole galaxy. Colour gradients are finally obtained by calculating the slope of the straight line that best fits the colours, \((m_1 - m_2)\), at different galactic radii (those for which a surface brightness profile is provided in the SDSS) versus the radii of the annuli normalized by the galaxy half light radius in the \( r \) band, \( R50:\)

\[
\nabla m_1 - m_2 = \frac{\Delta (m_1 - m_2)}{\Delta (R/R50)}.
\]

The normalization in radius is done in order to allow us to compare galaxies with different light distributions and sizes. The colour gradients of all the galaxies within the four studied luminosity-threshold samples have been obtained from the surface brightness profile out to the annulus containing the radius \( R = 2 \times R50 \). Thus, the radial coverage is consistent with previous studies. A further analysis on the effect of radial coverage is made in A2. In order to allow a fair comparison with recent literature we have also obtained colour gradients from the variation of internal colour with the logarithm of the normalized radius (colour per radial decade).

When computing the errors on the measured gradients we use a Monte Carlo method to take into account the observational errors in both the surface brightness and \( R50 \) measurements. Surface brightness values within a galaxy are related, with one value influencing the values at outer radii. In order to simplify the calculation we use a compromise by effectively considering the surface brightness values as independent and restricting the random values, obtained with the Monte Carlo method, within 1\( \sigma \). Thus, in order to include the observational errors, we repeat the whole process, except for the calculation of the (\( K + e \))-correction, 1000 times for each galaxy using each time a random value extracted from the error distribution for the variables within 1\( \sigma \) of the measurements, assuming that the initial errors have a Gaussian distribution.

We obtain the probability distribution from the Monte Carlo runs making use of a simple estimator\(^5\) and then we calculate the expected value of the colour gradient and its variance.

\[^4\] A taut spline is a piecewise cubic interpolant for which the first and last internal knots are not used. See de Boor (1978) for a full description.

\[^5\] The simple estimator, \( f \), is basically a weighted histogram without a dependency on the selection of the first bin, though it maintains a dependency on the step size, \( h \):

\[
f(x) = \frac{1}{n} \sum_{i=1}^{n} w \left( \frac{x - x_i}{h} \right).
\]

Here the weight, \( w \), is 0.5 if \( |x - x_i| < 1 \) and 0 otherwise.

3 RESULTS

Here we explore the origin of the colour gradient distribution in connection with the different classifications of galaxies into either early and late types or star forming, passively evolving and hosting nuclear activity.

We have calculated the gradients for the \((g - i)\), \((g - r)\), \((r - i)\), \((i - z)\) and \((r - z)\) colours. Fig. 3 shows the distribution of the \((g - i)\) and \((r - z)\) colour gradients for galaxies in sample S20.5. We have found that the distributions of the colour gradients in the \((g - r)\) and \((g - i)\) colours are similar. The distributions of the colour gradients in the \((r - i)\), \((r - z)\) and \((i - z)\) colours are also similar between them. As described in the introduction this is due to the similarity in the spectral characteristics that these colours probe.

Fig. 4 presents the dependency of the variance in the colour gradient with the actual values of the \((g - i)\) and \((r - z)\) colour gradients. From this figure we learn that galaxies with redder cores (negative colour gradient) measured from the \((r - z)\) colour gradients, tend to have larger errors, due to the \( z \) band being the noisiest.

![Figure 3. Distribution of \((g - i)\) (solid line) and \((r - z)\) (dot-dashed line) colour gradients for galaxies within the sample S20.5. Median colour gradient values are shown as short lines of the same type as their corresponding distribution. Histograms are normalized to give unit area underneath.](image)

![Figure 4. Distribution of colour gradients errors for \((g - i)\), left, and \((r - z)\), right, for galaxies in the S20.5 sample. Each contour represents a factor of 2 change in density.](image)
among the four in this study. The same is not true for the \((g - i)\) colour gradients. It can be seen in Fig. 4 that steeper gradients tend to have larger errors, for both colour gradients.

Fig. 3 shows that both the \((g - i)\) and \((r - z)\) colour gradients for sample S20.5 have median values that are similar: \(-0.048, -0.067\), respectively \((-0.187, -0.277)\) when defining colour gradients as colour per decade in normalized radius, in decimal logarithmic units. However, the distribution for the \((r - z)\) colour gradient presents a clear longer negative tail. This slight difference is likely to be due to the fact that redder stars contribute more in the \((r - z)\) than in the \((g - i)\) colour, giving rise to steeper gradients. However, the tilted distribution of the \((r - z)\) colour gradient variance shown in Fig. 4, would also be responsible, at least in part, for this difference.

We have also compared the distribution of colour gradients for the different luminosity-threshold selections defined in Table 1. There is not a clear change in the shape of the distributions for the different samples, just different numbers of galaxies. The change in median values from one sample to another is rather small: \(-0.050, -0.049\) and \(-0.044\) for the median \((g - i)\) colour gradient of samples S19, S20 and S21, respectively. When defining colour gradients as colour per decade in normalized radius we obtain the following median values \(-0.185, -0.194\) and \(-0.167\) for samples S19, S20 and S21, respectively. These last values are roughly in agreement with the Tortora et al. (2010) study, where they found a non-monotonic dependency of colour gradients with magnitude, when galaxies fainter than \(M_r = -20\) were considered.

In Appendix A we analyse some of the systematic effects that could affect the distribution of colour gradients, including the ellipticity, the amount of light considered in the calculation and the effect of having close pairs of galaxies. Considering the result found in Appendix A and the similar distributions for all the luminosity-threshold samples considered in this work, we can conclude that the results for the colour gradient distribution are robust. Returning to Fig. 3, we can clearly see there that galaxies tend to have small internal colour variation, resulting in quite flat colour gradients. Nevertheless, the median of the distribution is negative, implying that, in general, galaxy centres are redder than their outer parts. This agrees with previous studies using smaller samples of galaxies (see e.g. Peletier et al. 1990; Richard 2005; Lee et al. 2008; Tortora et al. 2010). As described in the introduction, Fig. 3 shows then that galaxies tend to have more metal rich cores that might also be hosting older stellar populations. Though, age gradients present larger dispersion than metallicity ones (MacArthur et al. 2009; Vlajić et al. 2009; Rawle et al. 2010; Tortora et al. 2010).

A remarkable feature of Fig. 3 is that the colour gradient distributions presents a single peak. This result could be indicating that galaxies with different structural characteristics, late and early-type galaxies, have undergone similar star formation histories. However, the distribution of colour gradients presented in Fig. 3 is much broader than a Gaussian. We have checked whether this is due to the observational errors using Monte Carlo simulations. We have found that taking into account the colour gradient variance, we still obtain a distribution narrower than the observed one. Thus, we demonstrate that the width and shape of the colour gradient distribution cannot be explained by the error distribution alone and that galaxies do indeed present different intrinsic colour gradients. We find the colour gradient distribution to be best described as the superposition of the distributions of two populations of galaxies.

We will explore further this last aspect in Sections 3.2 and 3.3. Before, we analyse the potentially different nature of those galaxies with extreme positive and negative colour gradients.

### 3.1 Positive and negative colour gradients

Here we study whether extremely steep colour gradients occur only in certain types of galaxies.

In Figs 5 and 6 we explore the possibility for galaxies with positive and negative colour gradients to separate in a colour–magnitude or colour–concentration parameter space. In both plots, density contours correspond to the behaviour of three subsamples separated by their \((g - i)\) colour gradient values. We have set as boundaries the

![Figure 5](image-url)

**Figure 5.** The upper panel shows the absolute magnitude in the \(r\) band versus the global colour \((g - r)\) for galaxies within the sample S19. Contours increase by factors of 2 in density, illustrating the behaviour of galaxies within different ranges of the \((g - i)\) colour gradient distribution. Dotted contours correspond to galaxies with \((g - i)\) colour gradients within the \(2\sigma\) limits of the total distribution. Solid/dashed contours present the distribution of those galaxies with their \((g - i)\) colour gradients above/below the \(2\sigma\) limit of the distribution, i.e. with bluer/redder cores than the average trend. The lower panel shows, in the corresponding line types, the medians and the distributions of the global \((g - r)\) colour for the three subsamples selected according to the \((g - i)\) colour gradients values. Histograms are normalized to give unit area underneath.

![Figure 6](image-url)

**Figure 6.** Similar to Fig. 5 but for \((u - r)\) versus concentration index.
2σ values corresponding to the \((g - i)\) colour gradient distributions of each sample. In this way we separate those galaxies with extreme colour gradients from the global trend.

Fig. 5 shows the absolute magnitude versus the global \((g - r)\) colour, while Fig. 6 presents \((u - r)\) versus light concentration. Both parameter spaces were explored by Blanton et al. (2003) and Driver et al. (2006), respectively. These studies showed the bimodality of galaxies, which separate in these spaces into early and late type.

In the Blanton et al. (2003) observations, the bimodality of SDSS galaxies is clear for galaxies fainter than \(M_B < -20\) (absolute magnitude at \(z = 0.1\)). A similar trend is found here for the faintest sample S19. The brighter samples, S20, S20.5 and S21, do not show a clear bimodality due to the magnitude cut.

In Fig. 5 those galaxies with very steep colour gradients only appear at the faint end, corresponding to the region with the largest dispersion, but also with the largest errors in magnitude. Galaxies with very steep positive and negative colour are distributed similarly in Fig. 5.

Fig. 6 shows that galaxies with extreme colours neither separate in this parameter space. The same is seen when defining the colour gradient as colour per decade in normalized radius. Nevertheless, Fig. 6 shows a remarkable behaviour: the galaxies with the steepest colour gradients are not galaxies with high concentration indices.

Galaxies with high concentration indices are generally passively evolving with minimal content of gas. Since few galaxies with high concentration index show steep colour gradients, then one expects that these steep colour gradients are more likely related to star formation. We will further explore this in Section 3.2.

From both Figs 5 and 6 it is clear that galaxies with steep colour gradients, independently of their sign, appear in larger numbers towards the blue end of both the \((u - r)\) and \((g - r)\) global colour distributions. Both figures show that redder and bluer cores appear within galaxies with similar global colours. However, for brighter samples, we find clearly that redder cores appear, on average, within redder galaxies than those with bluer cores. In particular, for the sample S20.5 those galaxies with extremely blue (red) cores have median global colours: \((g - r) = 0.82\) (0.85), \((u - r) = 2.3\) (2.4), while those galaxies with flatter colour gradients present the following median global colours: \((g - r) = 0.94, (u - r) = 2.8\).

We have also explored whether galaxies with very steep gradients appear separated when looking to parameter spaces that depend on age or metallicity against concentration index. In particular we have studied the variation with light concentration of the \(D4000\) spectral index and the Lick index \(H_\alpha\), both of which are mostly sensitive to age. We have also compared concentration to the Lick indices Mg2 and Fe5335, both closely related to the global metallicity of the galaxy.

We observe that both Fe5335 and \(H_\alpha\) present values that do not appreciably change with light concentration, which prevents the separation of galaxies in such parameter space. We find a similar bimodality in the parameter space \(D4000\) versus \(C\), to that reported by Kauffmann et al. (2003b) for the SDSS DR2. Moreover, we find that galaxies also separate into early and late types in the parameter space Mg2 versus \(C\). We find again that galaxies with very steep gradients appear to have a wide range of indices values, basically covering the same range as the global trend. It is also interesting to note that this is independent of the steep colour gradients being positive or negative. The lack of a clear locus occupied by those galaxies with steep gradients in the different studied parameter spaces suggest that the existence of extreme colour gradients depend weakly on the global age or metallicity of galaxies.

The studied indices are measured within the SDSS DR7 fibre spectra, with a diameter of 3 arcsec. We have explored how our results change depending on the amount of the galactic light that those 3 arcsec comprise. For this purpose, we have studied the behaviour of a subsample of galaxies with \(R50 < 1.7\) arcsec, i.e. galaxies with more than half of their light contained within the SDSS fibre spectra. This subsample exhibits similar tendencies to the global ones, except that in this case there are galaxies with steep colour gradients that have their light highly concentrated. A subsample of galaxies with only their cores measured within the SDSS spectra, with \(R50 > 4.6\) arcsec, give a better match to the global trends, in the sense that the light concentration distributes in a similar way to the total sample. We also find similar trends for the \(D4000\) versus \(C\), when using the spectral index derived by the MPA/JHU collaboration. Therefore, the tendencies of the colour gradients with the SDSS age and metallicity indices can be considered as representative of the tendencies with the global ages and metallicities of galaxies without making any further consideration.

We find that extreme internal colour variations tend to happen within galaxies that are blue, with low concentration indices and in the faint end of the sample distribution. Though, the difference between galaxies with extreme positive and negative colour gradients is small. This result implies that if the internal colour variation was mainly due to supernova winds or localized star formation regions, then the spatial probability for these phenomena to happen should be quite flat within galaxies. In their work on early-type galaxies Rawle et al. (2010) suggested that for galaxies with a velocity dispersion below 140 km s\(^{-1}\), metallicity gradients are tightly correlated with stellar mass, while above this threshold mergers are the main driver for setting the colour distribution within a galaxy. Thus, rather than a similar origin for blue and red cores, we could be looking to different phenomena: AGN or gas poor mergers versus gas rich mergers, occurring with a similar probability. All this points out the difficulty on disentangling how very steep gradients were originated. Further work will be needed to understand the similar distributions of positive and negative colour gradients.

### 3.2 Colour gradients within early and late-type galaxies

In this section we study the internal colour variation within early and late-type galaxies, using different parameters to classify galaxies into one of those categories.

The left-hand panel in Fig. 7 shows the variation of the \((g - i)\) colour gradient with the concentration index, \(C\), for galaxies in the S20.5 sample. As it can be seen in this plot, median colour gradients tend to be flatter for galaxies with higher values of the light concentration. In fact, the same is seen for all the studied colour gradients: \((g - i), (g - r), (r - z), (r - i)\) and \((i - z)\), in the different luminosity-threshold samples considered here. This was expected given the trends seen in the previous section. Due to the dispersion, this correlation is not statistically robust, with a Spearman coefficient of 0.19. However, the increase in the dispersion of observed colour gradients is not correlated with a trend in the error terms and so, it is significant.

We find that early-type galaxies tend to have flatter colour gradients than late-type galaxies. Most spirals are classified as late type and have an exponential light profile. In simple terms, these galaxies are formed by a bulge and a disc component. Bulges share features with early-type galaxies, being dominated by an old stellar population. Meanwhile, discs contain, in general, regions of star formation, providing an increase in the percentage of young stellar...
populations. These differences allow for greater colour variations to happen in comparison with early-type galaxies, whose characteristics are much more homogeneous.

Tortora et al. (2010) also found a similar trend for colour gradients with the Sérsic index, which is tightly related to the concentration index. These results also agree with the study by Weinmann et al. (2009), were they found that galaxies with $C \leq 3$ present steeper colour gradients.

Colour has also been widely used in the literature to split galaxies into early and late types. The middle panel in Fig. 7 shows the variation of the $(g - r)$ colour gradient with the global $(g - r)$ colour of galaxies. In agreement with Figs 5 and 6, it is clear in Fig. 7 that the redder a galaxy is the flatter the colour gradient is expected to be. The trend is similar to that seen for the concentration index: early-type galaxies present flatter colour gradients. However, the correlation with global colours is weaker than with the concentration index, with a Spearman index of $\sim 0.10$. This could indicate that colour gradients depend more strongly on morphological characteristics than on global colours. For example, if the colour gradient is set by the relative contribution of bulge and disc for late-type galaxies, one would expect that it would correlate more strongly with concentration index than with global colour.

For a given mass range, late-type galaxies are, in general, forming stars more efficiently than early-type ones. The right-hand panel in Fig. 7 presents the variation of colour gradient with the specific star formation derived by the MPA/JHU collaboration. With a Spearman index of $\sim 0.14$, the correlation between these two parameters is not statistically robust, likely due to the increase of the dispersion for those galaxies with higher specific star formation rates. The variance of the colour gradients does not determine the dispersion increase, which makes, again, the tendency significant.

Assuming a constant star formation, the inverse of the specific star formation, $M_*/SFR$, will provide an estimation of the time it took a galaxy to build up its observed stellar mass. Thus, higher values of specific star formation will correspond to younger galaxies, or at least, with a larger percentage of young stars. The found correlation between the specific star formation and the colour gradient indicates that steeper gradients appear for galaxies with higher percentages of young stars.

From Fig. 7 we can conclude that early-type galaxies have smaller internal colour variations compared to late-type galaxies.

We have also compared the shape of the distribution of colour gradients within early and late-type galaxies, selected accordingly to either concentration index, global colour or specific star formation, finding that early-type colour gradients have narrower distributions than late-types. As can be seen in Fig. 8 this is also true when separating galaxies into early and late-types using other parameters.

Fig. 8 shows the $(g - i)$ colour gradient distribution for galaxies from the S20.5 sample separated into early and late types following the Kauffmann et al. (2003b) work, by using the following parameters derived by the MPA/JHU collaboration: the $D_4000$ index, sampling the spectral 4000 Å break, the Balmer index $H_\lambda$ and the logarithmic stellar mass. Mass does not clearly separate galaxies into early and late types, but the characteristics of galaxies with masses below or above $10^{10.5}$ $M_\odot$ are rather different (Kauffmann et al. 2003b). Despite median values being quite close for early and late-type galaxies, it is apparent that late-type galaxies present a wider distribution with more extended tails than for the case of the early-type galaxies distribution.

As it is found here, Tortora et al. (2010) also reported a larger dispersion for colour gradients among late-type galaxies. Suh et al. (2010) found that although most of the early-type galaxies have quite flat colour gradients, there is $\sim 30$ per cent with residual star
formation that produces steeper colour gradients, in consonance with the distributions reported here.

Following Section 3.1, we have also studied here the relation between global galactic colours and the existence of extreme colour gradients within galaxies with low and high concentration indices. We find again that steep colour gradients appear within bluer late-type galaxies. However, in the case of early-type galaxies the global galactic colour does not appear to be correlated with the existence of extreme colour gradients.

When defining colour gradients as the variation of colour with the logarithm of the normalized radius, we obtain that early-type galaxies (C > 2.6) have a median (g − i) colour gradient of −0.13 for both the S19 and S20.5 samples, while late-type galaxies have median values of −0.27 and −0.32, for those two samples, respectively. The quoted values for early-type galaxies are smaller than those found by La Barbera et al. (2010). In the study from La Barbera et al. (2010), they apply two cuts in order to minimize the contamination of the early-type galaxy sample. Since we have only separated galaxies on basis of their concentration index values, we could have a larger fraction of late-type contaminants, providing steeper colour gradients than those reported by La Barbera et al. (2010).

In summary, the probability for finding strong internal colour variations within early-type galaxies is lower than for late-type galaxies.

3.2.1 Early and late type galaxies based on their colour gradients

Choi, Park & Vogeley (2007) have studied the behaviour of colour gradients with absolute magnitude for early and late-type galaxies, separated by their position in the colour gradient versus colour parameter space as defined by Park & Choi (2005). In order to compare our results with the Choi et al. (2007) study we have also separated galaxies into early and late type according to the Park & Choi (2005) method. Our definition of colour gradients is different since they just compare the light outside and inside half the Petrosian radius of galaxies. Moreover, they use magnitudes K-corrected to redshift 0.1. We have not applied any corrections to take into account these differences, we will thus compare tendencies qualitatively, rather than actual values.

The left-hand panel in Fig. 9 shows the (u − r) colour versus the (g − i) colour gradient, using black/grey dots for those early/late-type galaxies according to the Park & Choi (2005) criterion. In the same panel we have superimposed density contours for galaxies with different light concentrations: C ≤ 2.6 and C > 3. We can see there that the Park & Choi (2005) classification scheme agrees quite well with separations based on the concentration index.

The right-hand panel in Fig. 9 shows the (g − i) colour gradients as a function of absolute magnitude. Fig. 9 shows that those galaxies classified as early types have a very constant median colour gradient with absolute magnitude. The same behaviour is reported by Choi et al. (2007) and La Barbera et al. (2005), though other studies find some trends (see e.g. La Barbera et al. 2010). Early-type galaxies within the S19 sample, especially those fainter than $M_r \sim -21$, present values with increasing dispersion towards positive values, i.e. towards having bluer cores. This could be related to the branch of early-type galaxies with residual star formation, as the E+A galaxies, selected by Park & Choi (2005) method.

Indeed, in their work they showed that one of the advantages of their way of separating galaxies is that E+A galaxies are classified as early types, although they are bluer and less concentrated than most early-type galaxies. In fact, this increase in dispersion towards bluer cores within early types is the only difference found in the colour gradient versus absolute magnitude parameter space when using the concentration index to separate galaxies into early and late types.

Unlike global galactic colours, the internal colour variation do not relate clearly to the luminosity of galaxies, though median colour gradients tend to be steeper at brighter absolute magnitude bins. For fainter magnitudes than the ones studied here, Choi et al. (2007) observed that the colour gradients of late-type galaxies increase with magnitude. Nevertheless, within the magnitude range studied here the median colour gradients reported by Choi et al. (2007) also stay quite flat with magnitude. Bakos et al. (2008) studied the internal colour variation within 85 spiral galaxies finding that it is almost constant for a given luminosity.

In comparison to early types, late-type galaxies have steeper colour gradients and present a larger dispersion that increases for fainter magnitudes. These results are in agreement with Choi et al. (2007) and in consonance with our previous findings.

3.2.2 Velocity dispersion and stellar mass

Due to the complexity for obtaining the velocity dispersion, the SDSS provides measurements only for galaxies with a clean spectrum typical of an early type at $z < 0.4$. The subsample of galaxies with a reliable measurement of the velocity dispersion presents slightly flatter colour gradients with larger velocity dispersions. Such tendency is not statistically robust for the (g − i) colour gradient, with a Spearman index of ~0.12, due to the increase in dispersion. Though, as for the parameters studied before, the distribution of errors alone cannot explain the change in dispersion, recently ceased. See Yamauchi & Goto (2005) for a study of colour gradients in E+A galaxies.

6 E+A galaxies are dominated by an old stellar population but their spectra show signatures of the occurrence of minor star formation bursts that have
of mass for the colour gradient within late-type galaxies. As mention before, we find that the least massive galaxies in our sample present flatter median colour gradients, i.e. we find a very slight trend in the same direction as the one reported by Tortora et al. (2010). However, the slopes of these trends are different. The origin of this difference is unclear but it could be related with the different definitions of colour gradient or the sample selection.

3.3 Colour gradients, star formation and nuclear activity

Besides stellar winds and migrations, the nuclear activity could also be responsible for the existence of anomalous internal colour variations within galaxies. In fact, Menanteau et al. (2005) found one blue nucleated spheroid with star formation associated with the presence of an AGN.

Here we try to disentangle the effects of star formation and nuclear activity as responsible for setting colour gradients. We use the classification done by the MPA/JHU collaboration for the SDSS DR7 based on the one from Brinchmann et al. (2004), which makes use of the location of a galaxy in the parameter space log([O III]5007/Hβ) versus log([N II]6585/Hα), the so called BPT diagram (Baldwin, Phillips & Terlevich 1981), taking into account the S/N of the spectral lines. In this parameter space it is possible to separate star-forming galaxies from those with nuclear activity, though there is a region where galaxies are considered as composites. Due to the requirement of a minimum S/N value for the lines, not all galaxies can be classified following this scheme.

We have explored the locus occupied in the BPT diagram by those galaxies with very steep colour gradients, finding that they distribute following the mean trend.

Fig. 11 presents the distribution of the (g − i) colour gradients within galaxies from the S19 sample, separated into galaxies with nuclear activity and star-forming galaxies. The left upper panel of this figure presents the whole sample, showing that steep colour gradients are more likely to appear within star forming galaxies rather than those with nuclear activity. In fact, there is a minute increase, ∼2 per cent, in the percentage of galaxies classified as star forming among those with steep colour gradients, compared with the mean trend. This last tendency goes in the direction expected from the above discussions.
The studied early-type galaxies present a higher percentage of galaxies with nuclear activity, independently of their colour gradients. Thus, the top left-hand panel in Fig. 11 could be driven by the different distribution of colour gradients for early and late-type galaxies seen in Section 3.2.

The remaining panels in Fig. 11 explore the colour gradient distributions for galaxies within three mass ranges. Kauffmann et al. (2003c) found that different levels of nuclear activity appear in galaxies with different masses. Galaxies with masses below $10^{10} \, M_{\odot}$ could present a weak AGN, but not a strong one. In this mass range we observe that those galaxies from the S19 sample that are hosting an AGN present a higher percentage of bluer cores than those forming stars. The other studied samples of galaxies do not present this difference, but yet, they contain fewer low-mass galaxies. The observed trend could be explained if those weak AGNs were triggering star formation localized only in the central region of their host, or, more unlikely, if the AGN within these low-mass galaxies was driving dust out of the central galactic region, lowering its internal extinction, providing bluer cores.

Galaxies more massive than $10^{10} \, M_{\odot}$, host most of the AGN activity. As expected from Section 3.2.2, the colour gradient distribution for the most massive galaxies is quite narrow, with few galaxies presenting steep colour gradients. The median colour gradients for massive galaxies remain quite constant and comparable to the global median.

Our results suggest that nuclear activity is a marginal driver for creating steep colour gradients, and that it is overcome by the dependency between colour gradients and morphological type, at least for those galaxies with masses above $10^{10} \, M_{\odot}$.

### 3.4 Colour gradient change with redshift

Comparing the two panels in both Figs 5 and 6 for the samples under study, we have observed that galaxies with steep colour gradients tend to be redder when moving to samples including galaxies at higher redshifts. The global sample also gets redder when going from sample S19 to S20.5, but the variation is smaller. We have observed that colour gradients do not depend strongly on absolute magnitude, except for an increase in the scatter at the faintest end. Thus, this result could suggest a stronger evolution for those galaxies with steeper colour gradients in the recent past.

Fig. 12 shows the variation of the $(g-i)$ colour gradient with redshift for early and late-type galaxies within the S20.5 sample. For both types of galaxies the median colour gradients stay constant with the redshift, while the dispersion and errors increase. We find that for a fixed magnitude the dispersion in the colour gradient as a function of redshift is highly reduced. The opposite is not true. This is in agreement with Bakos et al. (2008).

We observe that it is more probable to find a galaxy with a steeper colour gradient at higher redshift. However, this trend of the dispersion could be driven by the errors distribution.

We have explored visually 48 early-type galaxies randomly selected among those with positive gradients, outside the 1σ dispersion range, and within the median value to explore the possibility of those early-type galaxies with steeper colour gradients to be more affected by artefacts. We find the same amount of galaxies either close to stars or other galaxies among both groups of galaxies. Thus, the observed tendency does not appear to be due to a higher presence of artefacts among those early types with steeper colour gradients.

In agreement with our study, La Barbera et al. (2003) found that colour gradients within spheroids are weakly dependent on the redshift, up to $z \sim 0.65$. Colour gradients within the discs studied by La Barbera et al. (2003) change appreciably from $z \sim 0$ to $z \sim 0.65$. However, this change is not so clear within the redshift limits used in our study.

The fact that median colour gradients do not appear to evolve at $z < 0.17$, points out that most of the star formation activity occurred previously.

### 4 SUMMARY AND CONCLUSIONS

In this paper we have studied the internal colour variation within galaxies from the SDSS DR7, with both clean photometry and spectroscopic measurements. We have obtained the global
(K + e)-correction by using SED templates from PEGASE and applied them to each galaxy in order to divide our initial sample into luminosity-threshold ones, with redshifts up to $z = 0.17$. These samples are the largest used for studying the internal colour variation in galaxies.

The internal colour variation has been quantified through the slope of the relation between radial colour and the galactic radius normalized to the one containing half the total galactic light, R50. Colour gradients have been obtained from the SDSS measurements of surface brightness circularly averaged in concentric annuli. Observational errors have been taken into account using a Monte Carlo method in the colour gradient calculation. This approach is independent of previous ones in the literature, therefore the agreement with earlier works underscores the robustness of the colour gradient as a useful parameter for studying particular aspects of galactic evolution.

In agreement with previous studies, we have found that colour gradients distribute around median values that are negative but close to zero, i.e. galaxies, independently of their morphological type, tend to have slightly redder cores than their external parts.

We have explored some of the possible systematics that could affect the measurement of the colour gradients. In particular we have explored the possible dilution due to the fact that we start our calculation of the colour gradient from a circularly averaged surface brightness profile. We observe that very elongated galaxies tend to have steep colour gradients, the opposite trend to the one expected if they were diluted. According to Choi et al. (2007), steep colour gradients within elongated galaxies are due to their internal dimming. In the calculation of the colour gradients we have left out the innermost annuli, since they are the ones most affected by seeing. We have explored the effect of obtaining colour gradients using different number of annuli, finding that for the range in which we work our results on colour gradients are robust. We find that galaxies with larger half light radii tend to have steeper colour gradients, being an intrinsic characteristic of galaxies and not an artefact.

We have selected a subsample of close pairs of galaxies that appear to be interacting. The sample is small, far less than 1 per cent of the total sample, and it represents an inferior limit of such close pairs of galaxies with respect to what the total percentage that might be found when considering the whole photometric SDSS sample. Despite the small number of galaxies in this sample, we find a larger proportion of galaxies with bluer cores here than in the whole population sample. As close pairs are more likely to be interacting and normally these interactions are associated with an enhancement of star formation, this supports the connection between steep colour gradients and recent bursts of star formation.

We find that the colour gradient distribution does not follow a Gaussian due to an excess of galaxies in the tails that cannot be explained alone by the errors distribution. A double-Gaussian fits better the colour distribution, pointing out a possible contribution of two distinctively different galaxy classes. Separating the initial sample of galaxies into early and late types we find that the distribution for colour gradients within late-type galaxies is more extended than that for early types. Nevertheless, the distribution of early-type galaxies is still broader than a Gaussian. We find this excess of steep colour gradients to be likely related to age gradients, AGN activity or an unusual dust content.

The observed distribution of colour gradients can be understood as a consequence of entangled effects. Gradients produced in mergers depend on the time scales that interplay in their creation and the mixing of elements that can contribute to their destruction. Galaxies observed at different epochs after a gravitational interaction can present colour gradients evolving with time. Nevertheless, even when observing galaxies at a similar time after a merger one expects to find a distribution of colour gradients and not a single value, since the metallicity enrichment appear to be highly non-uniform, due to the multiphase nature of the inter galactic medium (Springel & Hernquist 2003). Besides, Kobayashi (2004) simulated the formation of early-type galaxies through different kind of mergers, finding that the metallicity gradients (the main origin of colour gradients) strongly depend on the ratio of stellar masses and gas content between the progenitors. Moreover, even if early-type galaxies were formed in a 'monolithic collapse', for a given stellar mass there would be certain scatter in star formation efficiencies which provides a scatter in colour gradients (e.g Pipino et al. 2010). For late-type galaxies, the colour gradient dispersion is further enhanced due to the dust content and the bulge to disc relation depending on the observing inclination angle. The complicated patterns of stars migrations that follow the spiral arm formation can also enhance, at least temporally, this dispersion (Sánchez-Blázquez et al. 2009).

Galaxies with steep gradients share some global properties independently of presenting bluer or redder cores. Nevertheless, redder cores happen, on average, within galaxies redder than those with bluer cores. We have also observed that galaxies with high concentration values do not present steep colour gradients. It is known that mergers increase the galactic size and that galaxies with highly concentrated light have features indicating either a passive evolution in their recent past or the lack of gas, ruling out the possible existence of great internal colour variations. Thus, both results suggest the existence of a relation between colour gradients and the recent formation history of galaxies, in the sense that very steep colour gradients are likely related to recent star bursts.

We have found that galaxies with steeper colour gradients are more likely to be late-types according to either their structural parameters or to their specific star formation, i.e. a higher presence of young stars. It is interesting to note that we have found that colour gradients are less tightly related to global colours than the concentration index. Park & Choi (2005) found out that the parameter space colour–colour gradient could be very useful to select galaxies matching their optical morphology at low redshifts. Our study indirectly supports theirs, suggesting that colour gradients origins are more related to the recent formation history of galaxies, the kind of gravitational interactions recently suffered, than with the global galactic colours. Different studies (see e.g. Schawinski et al. 2009) are finding spheroidal galaxies with blue colours and red spirals. This proves the usefulness of a parameter like the colour gradient that is sampling something that cannot be seized through the global colour.

We have found that the possible correlation between colour gradients and nuclear activity is overcome by the stronger relation with galactic type, since nuclear activity appears more common among early types in our sample of galaxies.

At intermediate redshift, $0.37 < z < 0.83$, Menanteau et al. (2001) found that 30 per cent of field spheroids (classified based on their morphological parameters) show an unusual internal colour variation. Menanteau et al. (2001) associated this large colour variation with either star formation or AGN activity, in consonance with our results for a closer sample of galaxies.

Within the redshift range studied here, the colour gradients remain rather constant, implying that the studied galaxies had their last residual bursts of star formation at earlier times.

The results presented in this work agree with previous studies, though, here we are more dominated by the scatter due to the larger...
sample explored. Nevertheless, our results are very robust since they hold for the four studied luminosity-threshold samples. Colour gradients are normally defined in the literature as the colour variation as a function of the logarithm of the radius. Here we have used the variation of colour as a function of the radius itself. Using the former definition we have checked that we obtain qualitatively similar trends for colour gradients, except that their distribution covers a broader dynamical range. For the S20.5 sample, the median values of these distributions are $-0.187$ and $-0.277$, respectively for the $(r - z)$ and $(g - i)$ colour gradients. In our calculation of colour gradients we assume the observational errors in both colours and radii to be normally distributed. When using the logarithm of normalized radius, the error distribution deviates from a Gaussian. Thus, in order to make an accurate comparison we should modify the way we are including the observational errors in our calculation. This is likely to have a fundamental effect on the estimated errors, while colour gradients would remain practically unchanged. Leaving apart this issue, when defining the colour gradient as colour variation as a function of the logarithm of the radius we find qualitatively similar tendencies to the ones previously reported. The correlations appear stronger when defining colour gradients in this way, due to the enhanced dynamical range.

The fact that steep colour gradients are linked with a higher presence of young stars could provide an alternative method for exploring the interactions between galaxies. A thorough spectral analysis of those galaxies which present extreme colour variations could help us to better understand the mechanisms that generate either bluer or redder cores within galaxies.

ACKNOWLEDGMENTS

We thank J. Lucey, I. Ribas and R. Smith for their helpful comments. Thanks to C. Baugh for reading the manuscript. VGP is supported by a Science and Technology Facilities Council rolling grant. VGP and FJC acknowledge support from the Spanish Science Ministry by a Science and Technology Facilities Council rolling grant. VGP and FJC acknowledge support from the Spanish Science Ministry

REFERENCES

Abazajian K. et al., 2009, ApJS, 182, 543
Bakos J., Trujillo I., Pohlen M., 2008, ApJ, 683, L103
Baldwin J. A., Phillips M. M., Terlevich R., 1981, PASP, 93, 5
Begelman M., de Kool M. and Sikora M., 1991, ApJ, 382, 416
Blanton M. R. et al., 2003, ApJ, 594, 186
Brinchmann J., Charlot S., White S. D. M., Tremonti C., Kauffmann G., Heckman T., Brinkmann J., 2004, MNRAS, 351, 1151
Bruzual A. G. and Charlot S., 1993, ApJ, 405, 538
Charlot S., Worthey G., Bressan A., 1996, ApJ, 457, 625
Chiosi C., Carraro G., 2002, MNRAS, 335, 335
Choi Y.-Y., Park C., Vogeley M. S., 2007, ApJ, 658, 884
Clemens M. S., Bressan A., Nikola B., Rampazzo R., 2009, MNRAS, 392, L35
Cooper A. P. et al., 2010, MNRAS, 406, 744
de Boor C., 1978, A Practical Guide to Splines. Applied Mathematical Sciences. Springer, New York
De Lucia G., Springel V., White S. D. M., Croton D., Kauffmann G., 2006, MNRAS, 366, 499
Driver S. P. et al., 2006, MNRAS, 368, 414
Ferreras I., Lisker T., Pasqui P., Kaviraj S., 2009, MNRAS, 395, 554
Fioc M., Rocca-Volmerange B., 1997, A&A, 326, 950
Fukugita M., Shimasaku K., Ichikawa T., 1995, PASP, 107, 945
Hamilton D., 1985, ApJ, 297, 371
Hinkley S., Im M., 2001, ApJ, 560, L41

© 2010 The Authors, MNRAS 411, 1151–1166
Monthly Notices of the Royal Astronomical Society © 2010 RAS

SDSS DR7 colour gradients

Kauffmann G. et al., 2003a, MNRAS, 341, 33
Kauffmann G. et al., 2003b, MNRAS, 341, 54
Kauffmann G. et al., 2003c, MNRAS, 346, 1055
Kobayashi C., 2004, MNRAS, 347, 740
Ko J., Im M., 2005, J. Korean Astron. Soc., 38, 149
La Barbera F., de Carvalho R. R., 2009, ApJ, 699, L76
La Barbera F., Busarello G., Massarotti M., Merlini P., Mercurio A., 2003, A&A, 409, L21
La Barbera F., de Carvalho R. R., Gal R. R., Busarello G., Merlini P., Capaccioli M., Djorgovski S. G., 2005, ApJ, 626, 19
La Barbera F., de Carvalho R. R., de la Rosa I. G., Gal R. R., Swindle R., Lopes P. A. A., 2010, AJ, 140, 1528
Larson R. B., 1974, MNRAS, 169, 229
Lee J. H., Lee M. G., Park C., Choi Y.-Y., 2008, MNRAS, 389, 1791
Li Z., Han Z., 2007, A&A, 471, 795
MacArthur L. A., González I. J., Courteau S., 2009, MNRAS, 395, 28
Menanteau F., Abraham R. G., Ellis R. S., 2001, MNRAS, 322, 1
Menanteau F. et al., 2005, ApJ, 620, 697
Michard R., 2005, A&A, 441, 451
Oke J. B. and Sandage A., 1968, ApJ, 154, 210
Park C., Choi Y.-Y., 2005, ApJ, 635, L29
Peletier R. F., Davies R. L., Illingworth G. D., Davis L. E., Gawson M., 1999, AJ, 100, 1091
Pipino A., D’Ercole A., Chiappini C., Matteucci F., 2010, MNRAS, 407, 1347
Poggianti B. M., 1997, A&A, 122, 399
Rawle T. D., Smith R. J., Lucey J. R., 2010, MNRAS, 401, 852
Roche N., Bernardi M., Hyde J., 2009, MNRAS, 398, 1549
Roche N., Bernardi M., Hyde J., 2010, MNRAS, 407, 1231
Sánchez-Blázquez P., Gorgas J., Cardiel N., 2006, A&A, 457, 823
Sánchez-Blázquez P., Courty S., Gibson B. K., Brook C. B., 2009, MNRAS, 398, 591
Schawinski K. et al., 2009, MNRAS, 396, 818
Scodligio M., 2001, AJ, 121, 2413
Shimasaku K., 2001, AJ, 122, 1238
Spencer D. N., et al., 2003, ApJS, 148, 175
Spolaor M., Proctor R. N., Forbes D. A., Couch W. J., 2009, ApJ, 691, L138
Springel V., Hernquist L., 2003, MNRAS, 339, 289
Strateva I., 2001, AJ, 112, 1861
Strauss M. A. et al., 2002, AJ, 124, 1810
Stringer M. J., Benson A. J., 2007, MNRAS, 382, 641
Suh H., Jeong H., Oh K., Yi S. K., Ferreras I., Schawinski K., 2010, ApJS, 187, 374
Tamura N., Ohita K., 2003, AJ, 126, 596
Tamura N., Ohita K., 2004, MNRAS, 355, 617
Tortora C., Napolitano N. R., Cardone V. F., Capaccioli M., Jetzer P., Molinaro R., 2010, MNRAS, 407, 144
Vlajic M., Bland-Hawthorn J., Freeman K. C., 2009, ApJ, 697, 361
Weinmann S. M., Kauffmann G., van den Bosch F. C., Pasquali A., McIntosh D. H., Mo H., Yang X., Guo Y., 2009, MNRAS, 394, 1213
Worthy G., 1994, ApJS, 95, 107
Wu H., Shao Z., Mo H. J., Xia X., Deng Z., 2005, ApJ, 622, 244
Yamauchi C., Goto T., 2005, MNRAS, 359, 1557
York D. G., Anderson J. E., Jr, Anderson S. F., SDSS collaboration 2000, AJ, 120, 1579

APPENDIX A: POSSIBLE SYSTEMATIC EFFECTS IN THE COLOUR GRADIENTS

A1 Effect of the ellipticity

We obtain colour gradients from surface brightness measurements that are circularly averaged. Thus, colour gradients within elongated galaxies could be diluted. To address this issue we have separated galaxies within sample S20.5, the most populated one, into different ranges according to the ratio between the projected minor and major axes of the galaxies in the $r$ band, $b/a$. The top panel of Fig. A1

SDSS DR7 colour gradients
shows the variation of the \((g-i)\) colour gradient with \(b/a\). We can see that more elongated galaxies present steeper colour gradients, with median values varying from \(-0.07\) for galaxies with \(b/a < 0.4\) to \(-0.04\) for \(b/a > 0.8\). This tendency appears independently of the band used to define \(b/a\). The same tendency of steeper gradient for more elongated galaxies is found for galaxies in the other studied samples. It is also seen when colour gradients are defined as the variation of colour per logarithmic normalized radius. However, this is not observed for the \((r-z)\) colour gradients, where all median values are similar, \(\sim -0.07\), independently of their \(b/a\) value.

The bottom panel of Fig. A1 shows that the distribution of the error does not appreciably change as a function of the projected axial ratio. Thus, the error distribution is not enough to explain the slope change of the median values around \(b/a < 0.3\) seen in the top panel of Fig. A1.

This result shows that the dilution of colour gradients due to the use of circularly averaged surface brightness does not erase colour gradients although it may still dilute them somewhat.

Galaxies in the range \(b/a < 0.4\) are late types. Very inclined late-type galaxies are most affected by their internal absorption, something that could explain their steeper colour gradients. Due to their small gas content, early-type galaxies properties are not expected to be affected by their inclination.

Choi et al. (2007) studied the dimming effect for inclined late-type galaxies finding that it is better to exclude those with \(b/a < 0.6\) when studying properties that could be affected by galactic internal dimming. Considering only galaxies with \(b/a > 0.6\), we find that the linear variation of the median of the \((g-i)\) colour gradient with \(b/a\) has a slope smaller than \(0.02\), for all of the luminosity-threshold samples considered in our study. As expected from the large dispersion found in Fig. A1, the Spearman coefficient is too small to support statistically such a linear relation.

We can conclude that colour gradients do not vary in a significant manner with \(b/a\), except for very inclined late-type galaxies, which are most likely affected by their internal dimming. Since the \(z\) band is the least affected by dust extinction, this last result is consistent with the lack of \((r-z)\) colour gradient variation with \(b/a\).

Figure A1. Variation of \((g-i)\) colour gradients with \(b/a\) in the \(r\) band, top panel, and its errors, bottom panel, for galaxies within the S20.5 sample. In the top panel we have superimposed median colour gradients values and their 1\(\sigma\) dispersion range for \(b/a\) in the \(r\) band, circles with solid error bars, but also for \(b/a\) in the \(g\) band, triangles with dashed error bars. The bottom panel shows density contours with increments of a factor of 2.

Here we study the bias that we could be introducing by leaving out the innermost light, \(R < 0.67\) arcsec, of the galaxy. For all the studied galaxies, colour gradients have been obtained from the surface brightness within two times the radius containing the largest amount of galaxies have their half light radii within the two innermost annuli that we neglect computing the colour gradient. For the rest of the samples this does not occur. Moreover, in these samples less than 5 per cent of the galaxies have their half light radii within the first annuli considered in the calculation of colour gradients, \(0.67 < R_50 < 1.0\) arcsec (3rd annulus in the SDSS data base).

Fig. A2 shows the distribution of colour gradients of galaxies with \(b/a > 0.6\) from the S20 sample, divided in four ranges of half light radii. Fig. 1 shows that the largest amount of galaxies with \(b/a > 0.6\) from the S20 sample, divided in four ranges of half light radii. The cut in ellipticity allows us to isolate the tendency of colour gradients with \(R_50\). The ranges of \(R_50\) have been defined using as boundaries the outer radii of the 4th, 5th and 6th annuli in which the SDSS data base provides averaged surface brightness measurements. Fig. A2 shows that the largest amount of galaxies in sample S20 have their \(R_50\) within the 5th surface brightness annuli. This is also the case when considering all galaxies, independently of their ellipticity and it also holds for galaxies within the sample S20.5, while for sample S19 there is an even amount of galaxies with their \(R_50\) in either the 5th or 6th annuli. As it was pointed out before, all galaxies in our samples have at least four surface brightness measurements, from the 3rd to the 6th annulus. Thus, except for the S21 sample, when obtaining colour gradients we are taking into account surface brightness measurements both inside and outside \(R_50\). This point is essential for any robust conclusion about the behaviour of colour gradients.

Median colour gradients are steeper for higher values of \(R_50\) (arcsec), for all the defined luminosity-threshold samples. The same tendency has been found in the study by Roche et al. (2010) on early-type galaxies.
In Fig. A2 the ranges of values we study are defined by half light radii values in arcsec. Therefore, gradient values could be smeared out depending on the amount of light considered. To further explore this point, we have also studied the tendency of colour gradients when comparing galaxies with similar physical transverse radius, i.e. defining ranges of $R_{50}$ measured in $h^{-1}$ kpc. Different amount of surface brightness annuli account for a different amount of light for galaxies with similar sizes at different distances. Thus, in this way galaxies with colour gradients extracted from different amount of annuli are included in the same range.

Independently of the galactic ellipticity, the same tendency found for $R_{50}$(arcsec) applies when separating galaxies by their $R_{50}(h^{-1}$ kpc): the larger $R_{50}$ is, the steeper a colour gradient is likely to be. Galaxies within the S20.5 sample have median $(g-i)$ colour gradients: $-0.036$, $-0.048$, $-0.061$ and $-0.080$ for $R_{50}(h^{-1}$ kpc) $\leq 2$; $2 < R_{50}(h^{-1}$ kpc) $\leq 3$; $3 < R_{50}(h^{-1}$ kpc) $\leq 4$; $R_{50}(h^{-1}$ kpc) $> 4$, respectively. The same tendency for median values is found for galaxies within the S19 and S20 samples. In Fig. A3 we present the variation with $R_{50}(h^{-1}$ kpc) of the $(g-i)$ colour gradient and its error, for galaxies in S20. Median colour gradient values tend to decrease with larger half light radii, though, the correlation is dominated by the dispersion. When defining the colour gradient in decades of normalized radii (radius in logarithmic units), we also find that colour gradients get steeper for galaxies with larger $R_{50}$. Tortora et al. (2010) finds a similar tendency with effective radius, supporting the robustness of our result.

Dividing our sample into late and early types according to the concentration index, we found that the colour gradient of late-type galaxies change more rapidly with the galactic size than early type. The corresponding slopes for samples $S19$, $S20$ and $S25$ are: $-0.028$, $-0.025$ and $-0.024$ for late types and $-0.004$, $-0.002$ and $-0.002$ for early-type galaxies. The colour gradient of early-type galaxies, remains quite constant with galactic size.

For the samples of galaxies under study, the colour gradient variation with $R_{50}$ has been found to be independent of the amount of light used for obtaining it. Still, the deeming of colour gradients could be partly due to calculating them with fewer annuli with surface brightness measurements. If this was the case, we would expect a correlation between the gradient error and $R_{50}$(arcsec). However, no clear tendency is found, though the errors dispersion clearly decreases for larger $R_{50}$ (see Fig. A2). This tendency cannot explain alone the variation with $R_{50}$ seen for colour gradients. However, this consideration brings us to point out the unclear role that colour gradients could play in biasing global galactic properties obtained by extrapolating spectral characteristics from the SDSS galactic cores. In their studies, both Scodeggio (2001) and Roche et al. (2009) found out that the colour gradients should be taken into account for estimating the evolution of the colour–magnitude relation in early-type galaxies.

Despite the large dispersion in colour gradients values, the above results suggest that on average, galaxies with larger $R_{50}$, measured in either arcsec or kpc, intrinsically tend to have steeper colour gradients.

### A3 Effect of having close pairs of galaxies

Interacting galaxies can affect the colour gradients of each other (see e.g. Ko & Im 2005). Moreover, colour gradient can be ill defined for close pairs of galaxies. Besides, the sky subtraction for close pairs of galaxies within the SDSS data base may be problematic (John Lucey, private communication). Here we explore how the colour gradient distribute for close pairs of galaxies within our defined luminosity-threshold samples.

Fig. A4 shows the distribution of colour gradients for galaxies that are within 100 km s$^{-1}$ in redshift and within a projected radius of either 1 arcmin or 5 arcsec. This constitutes a lower limit to the fraction of close galactic pairs, since this number is expected to increase when including the whole photometric SDSS sample.²

We can observe that those close pairs with projected separations of maximum 1 arcmin, present a distribution with a median value coincident with that of the total sample. These are only 5 per cent of

² SDSS could not observe galaxies closer than 55 arcsec in the same plate and therefore close pairs are under represented in the spectroscopic sample. They were only observed in regions where spectroscopic plates overlapped.
the total $S20.5$ sample. Within the studied redshift range, 1 arcmin corresponds to around 100 kpc, approximately half the typical Virial radius of galaxies as massive as the Milky Way (Cooper et al. 2010). Thus, this will be an approximate limit to find interacting pairs of galaxies, which could affect each other colour gradients. Since no clear bias is found we do not have any further reason to consider that the colour gradients of close pairs of galaxies as far as 1 arcmin apart is ill defined.

In the $S20.5$ sample, we find 128 galaxies that are within 100 km s$^{-1}$ in redshift and 5 arcsec projected from another galaxy. A visual inspection of these galaxies reveals pairs of interacting galaxies, with some of them showing clear tidal tails. However, most of these close pairs appear just as red double nucleated structures, similar to that shown in the inset of Fig. A4.

It is very interesting to see in Fig. A4 that these galaxies tend to present bluer cores than what expected from the total sample. This result could point out that the star formation triggered by galactic interactions could be responsible for the observed bluer cores. Simulations such as the one from Kobayashi (2004) suggest that this phase will decay with time into a flatter colour gradient. In any case, these galaxies represent a percentage far below 1 per cent of the initial $S20.5$ sample, and, therefore their contribution to increase the presence of blue nucleated galaxies is negligible, at least in our sample.

This paper has been typeset from a \TeX/\LaTeX\ file prepared by the author.