Decomposing the productivity differences between hospitals in the Nordic countries

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Abstract Previous studies indicate that Finnish hospitals have significantly higher productivity than in the other Nordic countries. Since there is no natural pairing of observations between countries we estimate productivity levels rather than a Malmquist index of productivity differences, using a pooled set of all observations as reference. We decompose the productivity levels into technical efficiency, scale efficiency and country specific possibility sets (technical frontiers). Data have been collected on operating costs and patient discharges in each diagnosis related group for all hospitals in the four major Nordic countries, Denmark, Finland, Norway and Sweden. We find that there are small differences in scale and technical efficiency between countries, but large differences in production possibilities (frontier position). The country-specific Finnish frontier is the main source of the Finnish productivity advantage. There is no statistically significant association between efficiency and status as a university or capital city hospital. The results are robust to the choice of bootstrapped data envelopment analysis or stochastic frontier analysis as frontier estimation methodology.

Keywords Productivity · Hospitals · Efficiency · DEA · SFA

JEL Classification C14 · I12

1 Introduction

In previous studies (Kittelsen et al. 2009; Kittelsen et al. 2008; Linna et al. 2006, 2010) one has found persistent evidence that the somatic hospitals in Finland have a significantly higher average productivity level than hospitals in the other major Nordic countries (Sweden, Denmark and Norway).\(^1\) These results indicate that there could be significant gains from learning from the Finnish example, especially in the other Nordic countries, but potentially also in other similar countries. The policy implications could however be very different depending on the source of the productivity differences. This paper extends earlier work by, (1) decomposing the productivity differences into those that stem from technical efficiency, scale efficiency and differences in the possibility set (the technology) between periods and countries, and (2) exploring the statistical associations between the technical efficiency and various hospital-level indicators such as case-mix, outpatient share and status as a university or capital city hospital.

\(^1\) Although the Nordic countries also include Iceland, comparable data on Icelandic hospitals have not been available. In this article we will therefore use the term Nordic countries about the four largest countries.
Finally, (3) we examine the robustness of the results to the choice of method.

International comparisons of productivity and efficiency of hospitals are few, primarily because of the difficulty of getting comparable data on output (Derveaux et al. 2004; Linna et al. 2006; Medin et al. 2013; Mobley and Magnussen 1998; Steinmann et al. 2004; Varabyova and Schreyögg 2013). Such analyses often find quite substantial differences in performance between countries. Differences may be due to the dissimilar hospital structures and financing schemes, e.g. whether hospitals exploit economies of scale, have an optimal level of specialisation, or face high-powered incentive schemes that would encourage efficient production. Differences may also result from methodological problems. Cross-national analyses are often based on data sets that only to a limited extent are comparable—in the sense that inputs and outputs are defined and measured differently across countries. Our comparison gains validity from the existence of a Nordic standard for diagnosis related groups (DRGs) (Linna and Virtanen 2011). As described in the data section, the structure of the hospital sectors are broadly similar in the Nordic countries and the main differences are handled by assuming country specific production frontiers and variables in the analysis. It is, however, well known that the way we measure hospital performance may influence the empirical efficiency measures (Halsteinli et al. 2010; Magnussen 1996). In this article we will therefore use both the non-parametric data envelopment analysis (DEA) method and the stochastic frontier analysis (SFA) method, and provide evidence of the robustness of our results.

2 Methods

2.1 Efficiency and productivity

Efficiency and productivity are often used interchangeably. In our terminology productivity denotes the ratio of inputs and outputs, while efficiency is a relative measure comparing actual to optimal productivity. Since productivity is a ratio, it is by definition a concept that is homogenous of degree zero in inputs and outputs, i.e. a constant returns to scale (CRS) concept. This does not imply that the underlying technology is CRS. Indeed, the technology may well exhibit variable returns to scale (VRS), and equally efficient units may well have different productivity depending on their scale of operation, as well as other differences in their production possibility sets.

Most productivity indexes rely on prices to weigh several inputs and/or outputs, but building on Malmquist (1953), Caves et al. (1982) recognised that (lacking prices) one can instead use properties of the production function, i.e. rates of transformation and substitution along the frontier of the production possibility set, for an implicit weighting of inputs and outputs. We will use the term technical productivity to denote such a ratio of inputs to outputs where the weights are not input and output prices but rather derived from the estimated technologies.

This analysis departs from Farrell (1957) who defined (the input-oriented) technical efficiency as:

\[ E_{i}^{Tc} = \min \{ \theta | (\theta x_i, y_i) \in T^c \} \]  

Where \((x_i, y_i)\) is the input/output vector for an observation \(i\), and \(T^c\) is the technology or production possibility set for year \(t\) and country \(c\). For an input/output-vector \((x, y)\) to be part of the production possibility set, we need to be able to produce \(y\) using \(x\). As shown in Färe and Lovell (1978), this is equivalent to the inverse of the Shephard (1970) input distance function.

If there are variable returns to scale, Farrell’s measure of technical efficiency depends on the size of the observation, so that we can account for (dis)efficiencies of scale. The measure of technical productivity can, following Førsund and Hjalmarsson (1987), be defined by rescaling inputs and outputs:

\[ E_{i}^{\lambda Tc} = \min_{\theta} \{ \theta x_i, y_i \in \lambda T^c \}, \]  

where the convex cone of the technology \(\lambda T^c\), contains all input–output combinations that are a proportionate rescaling of a feasible point in the technology set \(T^c\). While this is formally identical to a “CRS technical efficiency” measure, our definition here is instead that the reference surface is a homogenous envelopment of the underlying technology. This is the same assumption normally used in Malmquist indices of productivity change, see e.g. Grifell-Tatjé and Lovell (1995).

Furthermore, it is not necessary to assume that the technologies of different countries and time periods are identical in order to compare productivity, as long as one has a common reference set. It is common to use a specific (base) time period as a reference, as in Berg et al. (1992):

\[ M_{ij}^T = \frac{E_{i}^{\lambda Tc}}{E_{j}^{\lambda Tc}}, \]  

which compares the productivity of two observations \(i\) and \(j\) using a fixed time period \(t\) as the reference, even if the observations \(i\) and \(j\) are from different time periods. A widespread alternative method is to construct geometric averages of indices based on consecutive time periods, as

\[ E_{i}^{Tc} = \min \{ \theta | (\theta x_i, y_i) \in T^c \} \]  

\[ E_{i}^{\lambda Tc} = \min_{\theta} \{ \theta x_i, y_i \in \lambda T^c \}, \]  

\[ M_{ij}^T = \frac{E_{i}^{\lambda Tc}}{E_{j}^{\lambda Tc}}. \]  

\[ \text{Førsund and Hjalmarsson (1987) used the symbols } e_1 \text{ for input technical efficiency, as did Farrell (1957), and } e_3 \text{ for technical productivity which they call “overall scale efficiency”}. \]
in Färe et al. (1994), which avoids the arbitrary choice of reference period \( t \), but instead introduces a circularity problem. The approach followed here is instead to use information from all time periods for the country specific productivity reference:

\[
T^c = \text{Env}(T^c)
\]

(4)

where Env() is the convex envelopment of the time specific technologies. Furthermore, to compare the productivity across countries we will need the envelopment of all time and country specific technologies:

\[
T = \text{Env}(T^c)
\]

(5)

The reference sets (4) and (5) are not themselves technologies, only envelopment of technologies, as are the convex cones (rescaled sets) \( \lambda T^c, \lambda T \). Analogous to (2), it is then possible to define the productivity levels relative to the country specific references and the pooled references as \( E_{ij}^{Tc} \) and respectively.

The country \( c \) specific Malmquist index of productivity change over time can then be defined as.

\[
M^c_i = \frac{E_{ij}^{Tc}}{E_{ij}^{T}},
\]

(6)

which normally is reported for two observation \( i \) and \( j \) of the same unit at two points in time. In this analysis we are primarily concerned with comparing observations from different units in different countries, and there is no natural pairing of \( i \) and \( j \). Edvardsen and Førsund (2003) develop and report geometric means of Malmquist indices between a unit in one country and all units in another country. We will instead take a simpler approach and report the productivity and efficiency levels of each unit and their country means.

2.2 Decomposition

As discussed e.g. in Fried et al. (2008), the Malmquist index can be decomposed in various ways, where the original decomposition is into frontier shift and efficiency change. When working in productivity and efficiency levels, the starting point is instead the decomposition of technical productivity into technical efficiency and scale efficiency:

\[
E_{ij}^{Tc} = E_{ij}^{T} E_{ij}^{Tc} = (TP_i = TE_i \ast SE_i),
\]

(7)

where the parenthesis denotes the conventional way of writing the technical productivity (TP) as the product of technical efficiency (\( TE_i = E_{ij}^{T} \)) and scale efficiency (\( SE_i = E_{ij}^{Tc} \)). By including the possibility of comparing productivity across both time and countries, this decomposition naturally expands into:

\[
E_{ij}^{T} = E_{ij}^{Tv} E_{ij}^{Tv} E_{ij}^{Tc} E_{ij}^{Tc} = (TTP_i = TE_i \ast SE_i \ast PP_i \ast CP_i),
\]

where we have decomposed the now total technical productivity (TTP) into technical efficiency (\( TE_i = E_{ij}^{Tv} \)), scale efficiency (\( SE_i = E_{ij}^{Tv} \)), period productivity (\( PP_i = E_{ij}^{Tc} \)) and country productivity (\( CP_i = E_{ij}^{Tc} \)). Each of these is specific to the observation \( i \).

Note that dividing this decomposition for two observations of one unit at different points in time, and ignoring the country productivity, one gets the common Malmquist decomposition of technical efficiency change, scale efficiency change and frontier change. As with the Malmquist index, the decomposition is not easily extended to comparisons between countries, as there is no natural pairing of observations. Asmild and Tam (2007) develop a global index of frontier shifts which they note would be useful for international comparisons, but does not extend this to a full decomposition.

These concepts are illustrated in Fig. 1, where we ignore the time dimension and concentrate on country differences. For an observation \( A \) in country 1 with a production possibility set bounded by the production function Frontier 1, we can define the technical efficiency by (1) above as the ratio \( BC/BA \) of necessary inputs to actual inputs for a given output. The productivity of \( A \) is the slope of the diagonal \( OA \), but we can normalise this in (2) by comparing it to the maximal productivity given by the slope of the diagonal OD. The technical productivity of \( A \) is then the ratio \( BD/BA \). Using the definition implicit in (7), scale efficiency is...
BD/BC. Assume that country 2 has a production possibility set bounded by Frontier 2, and that the maximal productivity of country 2 given by the slope OE is also the maximal for all countries, i.e. bounding the convex cone of all possibility sets $\lambda T_i$. This slope OE will serve as the reference for the total technical productivity defined in (8), which for observation A is given by BE/BA. The country productivity for observation A is then the ratio BE/BD.

With only one input and one output as in Fig. 1, one country will define the reference and all observations in each country will have the same country productivity. With two outputs as in Fig. 2, the convex cone of each country’s frontier $\lambda T_i$ can be drawn as the curved lines for a given level of the single input. The convex cone of all the country frontiers $\lambda T$ is represented by the dashed line which serves as the reference for total technical productivity defined in (8). If the country frontiers cross as in this example, the country productivities will depend on the output mix of the observation.

2.3 Cost efficiency and productivity

Finally note that since we have only one input in our data, cost minimization for a given input price is formally equivalent to input minimization. Thus cost efficiency, which is defined as the ratio of necessary costs to input costs, is also equivalent to technical efficiency. The decomposition of productivity and the Malmquist index is most often shown in terms of technical efficiency and technical productivity but could easily have been developed in terms of cost efficiency and cost productivity. Note that in the general multi-input case the numbers will differ in technical and cost productivity decompositions, but in our one-input case, the actual numbers will be identical. Thus, we may view the terms technical efficiency and cost efficiency as equivalent in discussing the results in this analysis.

2.4 Estimation method

The DEA and SFA methodologies build upon the same basic production theory basis. In both cases one estimates the production frontier (the boundary of the production possibility set or technology) or the dual formulation in the cost frontier, but the methods are quite different in their approach to estimating the frontiers and in the measures that are easily calculated and therefore commonly reported in the literature (Coelli et al. 2005; Fried et al. 2008). While the major strengths of DEA has been the lack of strong assumptions beyond those basic in theory (free disposal and convexity) and the fact that the frontier fits closely around the data, SFA has had a superior ability to handle the presence of measurement error and to perform statistical inference. The latter shortcoming of DEA has been alleviated somewhat with the bootstrapping techniques introduced by Simar and Wilson (1998, 2000).

In our data there are good reasons to choose either method. While the presence of measurement error is probably limited for those activities that are actually measured, there is a strong case for omitted variable (i.e. quality) bias that may be more severe in DEA. The DEA method can easily estimate the country specific frontiers without strong assumptions, thereby making country differences dependent on the input–output mix, while the SFA formulation generally introduces a constant difference between country frontiers. The presence of country dummies in SFA implies however, that information from other countries are used to increase the precision of the estimates and therefore the power of the statistical tests.

In the DEA analysis the frontiers have been estimated using the homogenous bootstrapping algorithm from Simar and Wilson (1998), while the second stage analysis of the statistical association of technical efficiency and the environmental variables has been conducted using ordinary least square (OLS) regressions. The SFA analysis has used the simultaneous estimation of the frontier component and the (in)efficiency component proposed in Battese and Coelli (1995).4

2.5 Data

Data has been collected for inputs and outputs of all public sector acute somatic hospitals. The hospital structure of the four Nordic countries is broadly similar. The structure

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3 In the general case with more than one output, cost efficiency and technical efficiency would be equal only if all units are allocatively efficient.

4 The DEA bootstrap estimations have been done in FrischNonParametric, while second stage regressions and the SFA analysis has been done in STATA 12 (StataCorp 2011).

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Fig. 2 The components of hospital total technical productivity in output–output space. For observation A in country 1, Total technical productivity (TTP) = OA/OD, Technical efficiency (TE) = OA/OC, and CP Country productivity (CP) = OC/OD
consists of mostly publicly financed and governed somatic hospitals with only a very few commercial hospitals, almost no specialization in medicine, surgical, cancer care etc., and no specialization to cater for specific groups such as veterans/military, childrens hospitals etc. Only in Finland are there a number of Health Centres with inpatient beds that serve less severe patients, and these are excluded from our analysis, as are the few commercial hospitals. Some non-profit private hospitals that are under contract with the public sector are included, however. The data includes almost the whole population of somatic hospitals in the Nordic countries, which due to a natural geographic monopoly usually serve a catchment area covering all residents. Differences in patient mix will mainly reflect demographic differences across the geographic areas, factors that are partly included in the second stage regression.

While the hospital sectors in all four countries are based on public ownership and tax-based financing, there are administrative and incentive differences. In Norway, all hospitals are state-owned, but the provision of hospital services is delegated to five (reduced to four during 2007) regional health enterprises (RHF). Each of these own between four and thirteen health enterprices (HF) which are the administrative units of hospital production, but a number of the health enterprises are multi-location institutions and the extent of integration between the actual physical hospitals varies considerably. In Denmark and Sweden hospitals are owned by the intermediate government level regions or counties (“regioner” and “landsting”), but single-location hospitals are still mainly separate institutions. The Finnish hospital sector is owned by health districts that are federations of municipalities. Norway and some counties in Sweden use partial activity based financing (ABF) based on the DRG-system, but with most of the payment made by block grants. In Denmark ABF was used only to a limited extent during the period. The Finnish hospital districts use various case-based classification systems (including DRGs) as a method of collecting payments from municipalities, but the Finnish payment system does not create similar incentives as ABF used in other countries (Kautiainen et al. 2011). However, since hospitals can be described by the same input–output vectors the productivity of the hospitals in our sample should be comparable even though they may not face the same production possibility sets.

Inputs are measured as operating costs, which for reasons of data availability are exclusive of capital costs. It was not possible to get ethical permission for the use of data for 2007 in Sweden. The Swedish data is further limited by the lack of cost information at the hospital level, necessitating the use of the administrative county (“landsting”) level as the unit of observation, each encompassing from one to five physical hospitals. The difference in level of observational unit between the countries (counties, health enterprises or hospitals) is one of the reasons why we estimate different technologies or production possibility sets in each country.

Since we do not have data on teaching and research output, the associated costs are also excluded. Costs are initially measured in nominal prices in each country’s national currency, but to estimate productivity and efficiency one needs a comparable measure of “real costs” that is corrected for differences in input prices.

To harmonize the cost level between the four countries over time we have constructed wage indices for physicians, nurses and four other groups of hospital staff, as well as one for “other resources”. This removes a major source of nominal cost and productivity differences between the countries, a difference that can not be influenced by the hospitals themselves, nor by the hospital sector as a whole. The wage indices are based on official wage date and include all personnel costs, i.e., pension costs and indirect labour taxes (Kittelsen et al. 2009). The index for “other resources” is the purchaser parity corrected GDP price index from OECD. The indices are weighted together with Norwegian cost shares in 2007. Thus we construct a Paasche-index using Norway in 2007 as reference point. Note that this represents an approximation, the index will only hold exactly if the relative use of inputs is constant over time and country.

Outputs are measured by using the Nordic version of the diagnosis related groups (DRGs). Each hospital discharge is assigned to one of about 500 DRGs on the basis of diagnosis and procedure codes. When activity is measured by DRG-points, discharges are weighed by a factor that is an estimate of the average cost of patients in that DRG. Thus the weighting is implicitly by patient severity or complexity as reflected in average costs. We define three broad output categories; inpatient care, day care and outpatient visits. Within each category patients are weighted with the Norwegian cost weights from 2007, where the weights are calculated from accounting data from a sample of major Norwegian hospitals.5 Outpatient visits were not weighted. Considerable work has gone into reducing problems associated with differences in coding practice, including moving patients between DRGs, eliminating double counting etc. The problem of DRG-creep, where hospitals that face strong incentives to upcode from simple to more severe DRGs based on the number of co-morbidities has been reduced by aggregating these groups. In the DEA analysis this had the effect of reducing the mean productivity level

5 From a common initial starting point, the Danish DRG system has diverged significantly from the other Nordic systems after 2002. Danish DRG-weights were used for the specific Danish DRG groups, while the level was normalized using those DRG-groups that were common in the two systems.
of Norwegian hospitals by 2 % points while the other 
countries were not affected, presumably because activity 
based financing is a more entrenched feature in Norway.

In addition to the single input and the three outputs, we 
have collected data for some characteristics that vary be-
tween hospitals within each country or over time, and that 
may be associated with efficiency. These include dummies 
for university hospital status which may capture any scope 
effects of teaching and research. This must be effects be-
ond the costs attributed to these activities which are al-
ready deducted from the cost variable, but the sign of the 
effect on productivity would depend on whether there are 
economies or diseconomies of scope between patient 
treatment and teaching and research. University hospitals 
may also have a more severe mix of patients within each 
DRG-group, which may bias estimated productivity 
downwards. The main case-mix effect should presumably 
already be captured by the DRG weighting scheeme. 
University hospitals are located in major cities. We also 
include a dummy for capital city hospitals, which may have 
a less favourable patient mix due to the socio-economic 
composition of the catchment area, so that one would ex-
pect the capital city hospitals to have lower productivity. 
However, university and capital city hospitals could also 
have lower costs due to shorter travelling times and a 
greater potential for daypatient or outpatient treatment, so 
the net effect is not obvious. Although all hospitals are 
located in towns, the university and capital city dummies 
should capture the main differences that may be due to 
urban or rural catchment areas.

The case-mix index (CMI) is calculated as the average 
DRG-weight per patient, and may again capture patient 
severity if the average severity within each DRG-group is 
correlated with the average severity as measured by the 
DRG-system itself, in which case one should expect a high 
CMI to be correlated with low productivity. The length of 
stay (LOS) deviation variable is calculated as the DRG-
weighted average LOS in each DRG for each hospital di-
vided by the average LOS in each DRG across the whole 
sample (i.e. expected LOS). Again this could capture dif-
fences in severity within each DRG group, but may also 
indicate excessive, and therefore inefficient, LOS. Finally, 
the outpatient share is an indicator of differences in treat-
ment practices across hospitals, where a high outpatient share 
may indicate lower costs per discharge. These variables are 
collectively termed “environmental variables”, although 
they are not always strictly exogenous to the hospital.

In earlier studies, the extent of activity based financing 
(ABF) has been an important explanatory variable, but in 
the period covered by our dataset there has been too little 
variation in ABF within each country. If a variable is or 
highly correlated with the country then it is not possible to 
statistically separate the effect from other country specific 
fixed effects. This also holds for structural variables such as 
ownership structure, financing system etc. Travelling time 
to hospital can be an important cost driver but is not in-
cluded here due to lack of data. Finally, no indicators of 
the quality of treatment have been available for this 
analysis.

Table 1 shows the distribution of hospitals between 
countries and summary statistics for the varibles in the 
analyses. When interpreting the size of the Swedish ob-
servations, remember that these are not physical hospitals 
but the larger administrative “Landsting” units. To a lesser 
extent, the Norwegian observations of health enterprises 
can also encompass several physical hospitals.

3 Results

3.1 DEA results

In the DEA analysis, the total technical productivity level 
is calculated with reference to a homogenous frontier es-
timated from the pooled set of observations for all coun-
tries and periods. Figure 3 show that the considerable 
productivity superiority of the Finnish hospitals found in 
previous studies is also present and highly significant in 
this dataset. The other Nordic countries are in some periods 
significantly different from each other, but in general have 
a similar productivity level.

Figure 3 also shows a slight time trend towards declin-


ging productivity. However, the DEA bootstrap tests did not 
reject a hypothesis of constant technology across time pe-
riods. This implies that we can ignore the time dimension 
and report the simpler three-way decomposition

\[
E_{iT} = E_T^{e_i} E_T^{ET} E_{iT}^{ET} = (TTP_i = TE_i \times SE_i \times CP_i),
\]

The productivity estimates for the individual observa-
tions are shown in Fig. 4. The hypothetical full produc-
tivity frontier is represented by productivity equal to 1.0, 
but since these numbers are bootstrapped estimates no 
observer is on the frontier. Clearly, the Finnish produc-
tivity level is consistently higher, with all Finnish ob-
servations doing better than most observations in Denmark 
and Norway and almost all in Sweden. Confidence inter-
vals are quite narrow so this is a robust result. In all 
countries one can see that smaller units tend to be more 
productive, while comparisons between countries are

\footnote{While we do not have data for travelling time in Denmark, we have 
calculated the average travelling time for the catchment area of emergency hospitals in the other countries. A separate analysis 
reported in Kalseth et al. (2011) indicate that travelling time can explain some of the cost differences between the Norwegian regions, but not a significant amount of the differences between countries.}
confounded by the fact that the Swedish units are not hospitals but observations on the administrative “Landsting” level.

Table 1 reports the mean country productivity results and its decomposition. The first line reports the of productivity of each country’s hospital sector relative to the

Table 1  Descriptive statistics. Observation means and SD

| Variable                          | Finland | Sweden | Denmark | Norway | Total |
|-----------------------------------|---------|--------|---------|--------|-------|
| Observation type                  | Hospital| Landsting/County | Hospital | Health enterprise |
| Number of observations            | 96      | 40     | 105     | 75     | 316   |
| Period                            | 2005–2007 | 2005–2006 | 2005–2007 | 2005–2007 |

Variables in production frontier function (deterministic part)

|                        | Finland | Sweden | Denmark | Norway | Total |
|------------------------|---------|--------|---------|--------|-------|
| Real Costs in billion NOK | 1112    | 4812   | 1516    | 1864   | 1893  |
| SD                     | 1563    | 5178   | 1167    | 1248   | 2488  |
| Outpatient visits      | 150,128 | 368,134 | 178,620 | 129,609 | 182,321 |
| SD                     | 170,646 | 445,542 | 125,012 | 70,008 | 212,219 |
| DRG points inpatients  | 22,516  | 65,262 | 22,517  | 31,447 | 30,047 |
| SD                     | 27,834  | 68,200 | 17,647  | 18,414 | 34,440 |
| DRG points daypatients | 3119    | 18,000 | 2651    | 4044   | 5067  |
| SD                     | 4092    | 18,207 | 2028    | 2532   | 8576  |

Variables in SFA efficiency part or DEA second stage (environmental variables)

|                                      | Finland | Sweden | Denmark | Norway | Total |
|--------------------------------------|---------|--------|---------|--------|-------|
| University hospital dummy            | 0.156   | 0.250  | 0.381   | 0.200  | 0.253 |
| SD                                   | 0.365   | 0.439  | 0.488   | 0.403  | 0.436 |
| Capital city dummy                   | 0.031   | 0.050  | 0.257   | 0.160  | 0.139 |
| SD                                   | 0.175   | 0.221  | 0.439   | 0.369  | 0.347 |
| Case mix index DRG patients          | 0.848   | 0.655  | 0.915   | 0.918  | 0.862 |
| SD                                   | 0.089   | 0.096  | 0.166   | 0.083  | 0.146 |
| Length of stay deviation             | 0.968   | 1.118  | 1.017   | 0.859  | 0.977 |
| SD                                   | 0.092   | 0.111  | 0.193   | 0.082  | 0.156 |
| Outpatient share                     | 0.841   | 0.731  | 0.865   | 0.773  | 0.819 |
| SD                                   | 0.028   | 0.049  | 0.044   | 0.026  | 0.061 |

Fig. 3 DEA bootstrapped productivity estimates by country and year with common reference frontier. Mean of observations and 95 % CI

Table 2 reports the mean country productivity results and its decomposition. The first line reports the of productivity of each country’s hospital sector relative to the
envelopment of the bootstrapped estimates of the country-specific production possibility sets, i.e. an estimate largely based on pooling the best hospitals. While Finland has an average productivity of around 80 % measured relative to the pooled frontier, the decomposition reveals that this is wholly due to lack of scale efficiency and technical efficiency, which are at around 90 % each. The country productivity mean is almost precisely 100 %, which means that it is the Finnish hospitals that define the pooled reference frontier alone.

For Sweden and Norway the picture is quite different; here the country productivity is the major component in the lack of total productivity. In fact, the cost efficiency and scale efficiency components are quite similar for Finland, Norway and Sweden. This implies that the hospitals in each country has a similar dispersion from the best to the worst performers both in terms of technical and scale efficiencies, but that the best performing hospitals in Norway and Sweden are significantly less productive than the best performers in Finland.

Denmark is in between, with significantly higher country productivity than Sweden and Norway, but still lagging far behind Finland. On the other hand, Denmark has clearly the lowest technical efficiency level of the Nordic countries, which means that the dispersion behind the frontier is largest in Denmark.
Table 2 also reports the scale elasticities in the last line. Scale properties can be different across geographical units, as also found in a study on hospitals in two Canadian provinces by Asmild et al. (2013). Since the DEA numbers are based on separate frontier estimates for each country, the fact that the units are of a different nature represents no theoretical problem but must be reflected in the interpretation of the results. For Finland, Denmark and Norway, where the units are hospitals or low-level health enterprises, the scale elasticities below 1 indicate decreasing returns to scale on average, a result that is often found in estimates of hospital scale properties. Thus, optimal size is smaller than the median size. For Sweden, however, the scale elasticity is larger than one, although only just significantly. Thus, even though the units of observation are clearly larger in Sweden, the optimal size is even larger. The natural interpretation of this paradox is that while the optimal size of a hospital is quite small, the optimal size of an administrative region (or purchaser), such as the Swedish Landsting, is quite large. Of course, other national differences that are not captured by our variables may also explain this result.

3.2 SFA results

The testing tree for the SFA model is shown in Table 3. The formulation by Battese and Coelli (1995) implies that factors that determine the position of the frontier function in the deterministic part of the equation are estimated

![Table 3](image)

| Parameter | SFA Frontier (deterministic component) | SFA Efficiency component | DEA Frontier distance | DEA Technical efficiency in second stage regression |
|-----------|--------------------------------------|--------------------------|----------------------|-----------------------------------------------|
| Finland   | 0.300*** (0.233–0.361) | 0.049 (−0.085–0.183) | 0.322*** (0.295–0.370) | −0.029 (−0.083–0.025) |
| Sweden    | 0.071 (−0.020–0.154) | −0.024 (−0.085–0.037) | −0.021 (−0.068–0.061) | 0.004 (−0.072–0.064) |
| Denmark   | 0.208*** (0.132–0.277) | −0.118*** (−0.174–(−0.062)) | 0.050*** (0.010–0.094) | −1.160*** (−0.246–(−0.075)) |
| Outpatient share | 0.658*** (0.259–1.057) | 0.666** (0.014–1.319) | 0.030 | 0.040 |
| Length of stay deviation | −0.063 (−0.142–0.015) | −0.138** (−0.263–(−0.013)) | 0.048 (−0.160–0.064) | 0.064 (−0.204–0.075) |
| Case mix index | −0.048 | 0.040 | 0.030 | 0.012 |
| Capital city dummy | −0.015–0.075 | −0.021−1.101 | −0.049–0.029 | −0.040–0.064 |
| University hospital dummy | −0.216 | 0.533** (0.104–1.002) | −0.504–0.072 |

* *, **, *** Significant coefficients at 10, 5 and 1 % level respectively. Reference units are hospitals in Norway in 2007 that are not in the capital and not university hospitals. The reference unit in SFA has a technical efficiency estimate of 0.9176. In the DEA model the distance between the frontiers is measured at the average product mix of Norwegian hospitals.
simultaneously as the variables in the “explanation” of the inefficiency term. Right hand side variables can potentially enter both components.

Clearly, the strongest result is that country dummies should enter the frontier term. This implies that there are highly significant fixed country effects that are not explained by any of our other variables, and that by the assumptions of the model specification the country dummy should primarily shift the frontier term. The functional form of the inefficiency term is not easily tested but the exponential distribution is the one that fits the data most closely. The functional form of the frontier function itself is, however, testable, and the simple Cobb-Douglas form is rejected in favour of the flexible Translog form. The time period dummies are also rejected in both terms, which mean that the period can be ignored as in the DEA case.

The normalized marginal effects are shown in Table 4 together with the corresponding DEA results. The full estimation results for the preferred model are included in Appendix 2. The normalization in Table 4 is done so that a positive coefficient shows the percentage point increase in the productivity level (or decrease in costs) stemming from a one per cent increase in the explanatory variable. The frontier and efficiency terms are shown in separate columns. For the DEA results, the marginal effects are dependent on the input–output mix, and the numbers shown are for the average Norwegian observation.

The results are generally very robust across methods. The Finnish hospitals are strongly more productive than the other countries. The Swedish and Norwegian frontiers are not significantly different from each other, while the Danish frontier is in between the Finnish and the Swedish/ Norwegian. In the efficiency term, the only significant country effect is that the Danish hospitals are less efficient. Of the environmental variables, the outpatient share has a significant positive effect on productivity while the LOS deviation has a weaker negative effect. The case-mix index and the dummies for university and capital city hospitals have no effect on costs. There seems to be no sign that the central hospitals have a more costly case mix than what is accounted for by the DRG system.

4 Conclusion

International comparisons can reveal more about the cost and productivity structure of a sector such as the somatic hospitals than a country specific study alone. In addition to an increase in the number of observations and therefore in the degrees of freedom, one gets more variation in explanatory variables and stronger possibilities for exploring causal mechanisms. This study has found evidence of a positive association between efficiency and outpatient share, a negative association with LOS, and no association with the case-mix index or university and capital city dummies. We have further found evidence of decreasing returns to scale at the hospital level, with a possibility of increasing returns to scale at the administrative or purchaser level. There is also evidence of cost/technical inefficiency, particularly in Denmark.

As so often, the strongest results are not what we can explain, but what we cannot explain. There is strong evidence, independent of method, that there are large country specific differences that are not correlated with any of our other variables. Finland is consistently more productive than the other Nordic countries. There are systematic differences between countries that do not vary between hospitals within each country. Without observations from more countries, or more variables that vary over time or across hospitals within each country, such mechanisms cannot be revealed by statistical methods.

On the other hand, qualitative information can give some speculations and plausible explanations. Interestingly, the stronger incentives that are supposed to be provided by ABF in Norway and some counties of Sweden does not seem to increase productivity. These data are from before the financial crisis, but Finland was still suffering the aftereffects of a local recession after the collapse of the Soviet Union, with increased budget restraint in the public sector. Based on interviews of 8 hospitals in Nordic countries (Kalseth et al. 2011) some of the possible reasons for the Finnish good results can be the good coordination between somatic hospitals and primary care, including inpatient departments of health centres. This coordination is primarily due to the common ownership by the municipalities of both hospitals and primary care institutions. Finland also had a smaller number of personnel as well as better organization of work and team work between different personnel groups inside hospitals (Kalseth et al. 2011). However, these findings are still preliminary. An important research and policy question is whether the higher productivity in Finland is related to differences in quality.

Our claim is that the country productivity differences are consistent with possible differences in system characteristics that vary systematically between countries. Such characteristics may include the financing structure, ownership structure, regulation framework, quality differences, standards, education, professional interest groups, work culture, etc. Some of these characteristics, such as quality, 7 As mentioned, Finland has low-speciality health centres that are excluded from study. If these treat the least severe patients then the Finnish hospitals would have a more severe case-mix. Most of this should be captured in the DRG-system, but if hospital patients are more severe within each DRG the potential bias is that the Finnish hospitals are actually even more productive than estimated here.
may also vary between hospitals in each country and should be the subject of further research.

Differences in estimated country productivity are also consistent with data definition differences, but the analysis in Kalseth et al. (2011) does not support this. In summary, these country effects are essentially not caused by factors that can be changed by the individual hospitals to become more efficient, but rather factors that must be tackled by relevant organizations and authorities at the national level.

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Appendix 1: Estimated models

Let \( x_i \) denote the level of the single input for each hospital \( i \) and \( y_n \) is the vector of \( y_{ni} \), the level of output \( n \) for hospital \( i \). The environmental variables that enter the frontier function are denoted \( z_{di} \), and the environmental variables that enter the (in)efficiency function \( z_{di}^b \). After the tests described in Table 3, \( z_{di}^b \) only consists of country dummies (with Norway as the dropped reference), while \( z_{di}^b \) consists of all variables in the first column of Table 4.

The set of observed hospitals \( i \) in each country \( c \) and period \( t \) is denoted \( H_{ct} \), the intertemporal set in each country is \( H_c = \bigcup_i H_{ct} \), and the full set of all observations across all countries is \( H = \bigcup_c H_c \).

DEA estimates

For an input–output vector \( (x_0, y_0) \), the basic estimates of country-and period-specific technical input efficiencies used in Table 1 are bootstrapped estimates using the standard DEA variable returns to scale (VRS) formulation:

\[
E_T^{0c} = \min \left\{ \theta \left| \theta x_0 \geq \sum_{i \in H^c} \lambda_i x_i, y_0 \leq \sum_{i \in H^c} \lambda_i y_i, \sum_{i \in H^c} \lambda_i = 1 \right. \right\}
\]

(10)

Where the restrictions represent the DEA estimate of the production possibility set \( T^c \). The period- and country-specific technical productivity is then the measured relative to the homogenous envelopment \( \lambda T^c \) of the set:

\[
E_T^{0c} = \min \left\{ \theta \left| \theta x_0 \geq \sum_{i \in H^c} \lambda_i x_i, y_0 \leq \sum_{i \in H^c} \lambda_i y_i \right. \right\}
\]

(11)

The estimate of productivity of an observation relative to the intertemporal country-specific frontier is calculated relative to a reference set pooling all observations in each country across periods:

\[
E_T^{0T} = \min \left\{ \theta \left| \theta x_0 \geq \sum_{i \in H} \lambda_i x_i, y_0 \leq \sum_{i \in H} \lambda_i y_i \right. \right\}
\]

(12)

The estimate of productivity of an observation relative to the intertemporal and cross-country frontier, i.e. the total technical productivity is calculated relative to a reference set pooling all observations across all countries and periods:

\[
E_T^{0T} = \min \left\{ \theta \left| \theta x_0 \geq \sum_{i \in H} \lambda_i x_i, y_0 \leq \sum_{i \in H} \lambda_i y_i \right. \right\}
\]

(13)

After elimination of the assumption of period-specific frontiers from the decomposition (9), technical efficiency is calculated with the intertemporal pooled country reference sets:

\[
E_T^{0} = \min \left\{ \theta \left| \theta x_0 \geq \sum_{i \in H} \lambda_i x_i, y_0 \leq \sum_{i \in H} \lambda_i y_i, \sum_{i \in H} \lambda_i = 1 \right. \right\}
\]

(14)

All estimates are bootstrapped using the homogenous procedure in Simar and Wilson (1998), with 2000 bootstrap iterations and kernel estimates of the inefficiency distributions based on the technical efficiency scores (10) and (14) respectively.

The second stage regression in the DEA analysis is an OLS regression with bootstrapped technical efficiency estimates \( \hat{E}_i^T \) for each hospital \( i \) as the dependent variable and environmental variables \( z_{di}^b \) independent variables of the form:

\[
\hat{E}_i^T = \gamma_0 + \sum_{t=1}^T \gamma_{t} z_{d_{it}} + \epsilon_i
\]

(15)

SFA estimates

The stochastic frontier analysis is based on maximum likelihood estimation of the Battese and Coelli (1995) type.
of model with the variance of the inefficiency term is a function of the environmental variables. The model is estimated using the “cost function” procedure in Stata 13 as our only input is total operating costs. After the tests in Table 3, the reported results are from a model with a translog functional form for the deterministic part and exponential distribution for the inefficiency term.

\[
\ln x_i = \beta_0 + \sum_{n=1}^{N} \beta_n \ln y_{ni} + 0.5 \sum_{n=1}^{N} \sum_{m=1}^{N} \beta_{nm} \ln y_{ni} \ln y_{mi} \\
+ \sum_{k=1}^{K} \eta_k z_{ki} + v_i - u_i v_i \sim \text{Normal}(0, \sigma_v^2) \\
u_i \sim \text{Exponential}(\sigma_{ui}) , \quad \ln(\sigma_{ui}^2) = \delta_0 + \sum_{l=1}^{L} \delta_l z_{li}^b \quad (16)
\]

### Appendix 2: Raw coefficients in SFA analysis

See Table 5.

| Table 5 | SFA-analysis with an exponentially distributed efficiency component |
|---------|-------------------------------------------------|
| Coefficient | Z-value |
| Cost frontier (deterministic part) | |
| Constant | -10.349 | -9.760*** |
| Ln DRG outpatients | 0.410 | 0.930 |
| Ln DRG inpatients | 0.093 | 0.260 |
| Ln DRG daypatients | 0.500 | 2.090** |
| (Ln Outpatients)* (Ln DRG inpatients) | -0.246 | -2.030*** |
| (Ln Outpatients)* (Ln DRG daypatients) | 0.030 | 0.510 |
| (Ln DRG inpatients)* (Ln DRG daypatients) | -0.240 | -2.690*** |
| (1/2) (Ln Outpatients)² | 0.193 | 1.940* |
| (1/2) (Ln DRG inpatients)² | 0.530 | 2.760*** |
| (1/2) (Ln DRG daypatients)² | 0.200 | 3.650*** |
| Finland | -0.356 | -7.660*** |
| Sweden | -0.074 | -1.540 |
| Denmark | -0.233 | -4.970*** |
| Inefficiency part | |
| Constant | 5.457 | 1.470 |
| Finland | -1.236 | -0.720 |
| Sweden | 0.610 | 0.770 |
| Denmark | 2.984 | 4.120*** |
| Outpatient share | -16.634 | -3.230*** |
| Length of stay deviation | 1.602 | 1.580 |
| Case mix index | 1.214 | 0.840 |
| Capital city dummy | -0.755 | -1.290 |
| University hospital dummy | 0.244 | 0.480 |

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