Indirect reciprocity is sensitive to costs of information transfer

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How natural selection can promote cooperative or altruistic behavior is a fundamental question in biological and social sciences. One of the persuasive mechanisms is "indirect reciprocity," working through reputation: cooperative behavior can prevail because the behavior builds the donor's good reputation and then s/he receives some reciprocal benefits from someone else in the community. However, an important piece missed in the previous studies is that the reputation-building process requires substantial cognitive abilities such as communication skills, potentially causing a loss of biological fitness. Here, by mathematical analyses and individual-based computer simulations, we show that natural selection never favors indirect reciprocal cooperation in the presence of the cost of reputation building, regardless of the cost-to-benefit ratio of cooperation or moral assessment rules (social norms). Our results highlight the importance of considering the cost of high-level cognitive abilities in studies of the evolution of humans' and animals' social behavior.
fitness defined as the total payoff during the generation (i.e., natural selection). Higher fitness implies a higher probability that the individual can leave more offspring.

How does an observer build the donor’s reputation? In other words, what behavior of the donor is interpreted as good or bad? We assume that an observer builds the donor’s reputation based on the donor’s own reputation and behavior and the opponent’s reputation14, and that all individuals in the population share the same moral assessment rule16–18 (see Methods). Furthermore, each individual’s reputation at the initial round is assumed to be good.

In the present study, as in the previous studies8–16,17, we assume that each individual makes decisions in the prisoner’s dilemma game based on the opponent’s reputation. Such a decision-making rule, called a behavioral strategy, is denoted by a two-dimensional vector, \( p = (p_B, p_C) \), where \( p_B \) and \( p_C \in [0,1] \) indicate the probability that the individual cooperates when his/her opponent’s reputation is bad and good, respectively. In addition, each individual in the role of the observer decides whether to build and spread the reputation of the donor. By \( q \in [0,1] \), we denote the probability that the individual builds the donor’s reputation. That is, each individual’s strategy is defined as a pair of \( p \) and \( q \), indicated by \((p, q)\).

Let \( G_t(p, q) \) be the fraction of individuals among \((p, q)\) strategists whose reputation is good at round \( t \), and let \( x(p, q) \) be the probability density of \((p, q)\) strategists over the population. Then, the average payoff of \((p^*, q^*)\) strategists at round \( t \) is:

\[
\pi_t(p^*, q^*) = b \int p \left(1 - G_t(p^*, q^*) \right) G_t(p^*, q^*) x(p, q) dp dq - c p^* \left(1 - G_t(p, q) \right) - c_B q^*,
\]

where \( G_t = \int G_t(p, q) x(p, q) dp dq \) denotes the fraction of individuals whose reputation is good in the whole population. The first term of equation (1) represents the benefit of cooperation multiplied by the probability that the focal \((p^*, q^*)\) strategist is cooperated with by other individuals; the second term denotes the cost of cooperation multiplied by the probability that s/he cooperates, and the third term is the cost of reputation building multiplied by the probability that s/he builds the donor’s reputation when s/he is in a role of an observer.

Since we can show that the reputation dynamics, \( G_t(p^*, q^*) \), depends on \( p^* \), but not on \( q^* \), for any moral assessment rules11–14 (see Methods), \( G_t(p^*, q^*) \) in equation (1) can be replaced by \( G_t(p^*) \), that is:

\[
\pi_t(p^*, q^*) = b \int p \left(1 - G_t(p^*) \right) G_t(p^*) x(p, q) dp dq - c p^* \left(1 - G_t(p, q) \right) - c_B q^*,
\]

where \( G_t(p^*) \) is the payoff to the observer in the prisoner’s dilemma game, which depends on \( p^* \) but not \( q^* \), and \( c_B q^* \) denotes the cost of reputation building, which depends on \( q^* \) but not \( p^* \).

Equation (3) indicates that, given a value of \( p^* \) individuals with \( q = 0 \) always get the highest payoff in each round, regardless of the cost-to-benefit ratio of cooperation \((c/b)\), the amount of the cost of reputation building \((c_B > 0)\), or the moral assessment rules (update rule of \( G_t(p, q) \)). This means individuals with \( q = 0 \) always get the highest fitness, sum of the payoffs, for any \( p \). In other words, natural selection always favors individuals who never build and spread a reputation (i.e., \( q = 0 \)) for any behavioral strategies, \( p \). Note that this statement is also true when we assume more general behavioral strategies, that is, when individuals make decisions based not only on the opponent’s reputation but also on their own reputation (see Methods)16–18. In summary, we show that, in the presence of the cost of reputation building, natural selection results in a society where no individual builds a reputation and thus indirect reciprocity never works.

To further explore the effect of the cost of reputation building in more complicated situations, we constructed an individual-based computer simulation model. Let us consider a population of \( n \) individuals. As in the seminal work on indirect reciprocity4, each player has a reputation score, \( s \), that ranges from \(-5\) to \(5\). At the beginning of each generation, which comprises \( m \times n \) consecutive rounds, scores are reset to zero.

In each round, three individuals are chosen randomly from the population: one is a potential donor of help, another is a potential recipient of the help, and the third is an observer. A potential donor decides to either give help (cooperation) or to refuse help (defection). Cooperation confers a benefit, \( b \), to the recipient while accruing a cost, \( c \), to the donor \((b > c > 0)\). Defection yields nothing to either person. Note that we assume that, with the probability \( \varepsilon (0 < \varepsilon < 1) \), an individual who intends to cooperate fails to cooperate because of, for example, a lack of resources or a mistake, called an implementation error9,16–19. After this, the observer decides whether or not to update and spread the donor’s reputation score (i.e., reputation building) with a cost \( c_R > 0 \).

As in the analytical model, we assume all individuals in the population share the same moral assessment rule (social norm). We consider the following three rules. One is the simple, called SCORING9, in which the reputation score increases by one unit if a potential donor cooperates; it decreases by one unit if s/he defects. That is, cooperation and defection are judged as good and bad, respectively. Another rule is MILD (or sometimes called STANDING)16,18–20: the score increases if a donor defects against a bad individual \((s < 0)\) or cooperates; it decreases otherwise. This rule incorporates the concept of justified defection16–18 and has been known to stabilize the indirect reciprocal cooperation16,18–20. The third rule is STEM (or sometimes called KANDORO)16,21: the score increases if a donor cooperates with a good individual \((s > 0)\) or defects against a bad individual; it decreases otherwise. This includes not only the concept of justified defection but also unjustified cooperation (i.e., cooperation with a bad individual is regarded as bad)16–18.

A donor’s behavioral strategy is given by a number, \( k (k = -5 \text{ to } 6) \): an individual with this strategy, \( k \), cooperates if the score of the recipient is at least \( k \). In other words, a high reputation score of an individual often implies a higher probability that others will cooperate with the individual. An observer’s strategy is depicted by a number, \( q \in \{0,1\} \): an individual with \( q = 1 \) (0) does (does not) update and spread the donor’s reputation score based on the moral assessment rule. That is, each individual’s heritable traits are \( k \) and \( q \).

At the end of each generation, each individual leaves offspring depending on his/her fitness (i.e., natural selection). The fitness value is defined as the total payoff received during the generation \((m \times n \text{ rounds})\). Higher fitness implies a higher probability that the individual can leave offspring. We use the “binary tournament selection” procedure, a genetic algorithm, to select individuals22. In addition, mutation is introduced: with the small probability \( \mu \), each individual’s strategy \( k \) and \( q \) changes to another value randomly.

Consistent with the previous studies9–18, we find that, in the absence of cost of reputation building, the frequency of cooperation increases with the decrease in the cost-to-benefit ratio of cooperation and the increase in the number of rounds in a generation (see the black points in Fig. 1). This tendency is common to all the three moral assessment rules (compare the panels A vs. B vs. C in Fig. 1). This indicates that the evolution of indirect reciprocal cooperation becomes easier as the net benefit of cooperation and the number of interactions among individuals increase.

However, the presence of the cost of reputation building completely destroys indirect reciprocal cooperation regardless of the cost-to-benefit ratio of cooperation or moral assessment rules (see the red points in Fig. 1). Even when the amount of cost of reputation building
is only 1% of the benefit of cooperation, the evolution of cooperation is impossible (red squares in Fig. 1). We also examined another case in which the reputation of a donor is built by the recipient instead of a third person/observer. That is, the recipient decides to or not to incur a cost of building the reputation of the donor. We confirm that, consistent with the original case, introducing the cost of reputation building makes it impossible (see Suppl. Fig. S1).

We also investigated a situation in which an observer who does not build the donor’s reputation can lose his/her own good reputation. In other words, individuals who do not incur a cost of reputation building can be judged as bad. We assume that, at each round, in addition to a donor, a recipient and an observer, one individual is selected as an observer of the observer, who we call a “second-order observer.” S/he decides whether or not to update and spread the observer’s reputation score with a cost $c_R > 0$. A second-order observer’s strategy is depicted by a number, $r \in \{0, 1\}$: an individual with $r = 1$ (0) does (does not) build the observer’s reputation. When a second-order observer’s strategy is $r = 1$, the (first-order) observer’s reputation score increases by one unit if s/he builds the donor’s reputation; it decreases by one unit otherwise. The results of the computer simulation show that, consistent with the original case, natural selection never leads to indirectly reciprocal cooperation regardless of the cost-to-benefit ratio of cooperation or moral assessment rules (see Suppl. Fig. S2), except for the unrealistic case without the cost of reputation building for second-order observers (i.e., $c_R = 0$; see the black points in Suppl. Fig. S2). This is because individuals building a reputation as a second-order observer (i.e., $r = 1$) are exploited by individuals with $r = 0$ for the cost, $c_R$ (see Suppl. Fig. S3).

These results together demonstrate that, as predicted by the analytical models, the evolution of cooperation based on indirect reciprocity is extremely vulnerable to the cost of reputation building in a complicated situation (e.g., a reputation score is 11-scale but not binary).

Discussion
We have examined the effect of the cost of reputation building on the evolution of cooperation through indirect reciprocity. By analytical investigation and individual-based computer simulations, we have shown that the slight cost of reputation building completely destroys indirect reciprocal cooperation regardless of the cost-to-benefit ratio of cooperation or moral assessment rules.

In a broad sense, our results are closely related to the second-order free rider problem24,25, which asks “who incurs a cost to preserve social systems for the maintenance of cooperation?”. A typical example is the evolution of altruistic punishment, which asks26–28 “who bears a cost of the punishment of defectors?”. Imagine that there are three types of individuals: free riders (defectors), altruistic punishers (cooperators who punish free riders) and cooperators who do not punish, and that there is a cost to administering punishment. In this situation, although altruistic punishers punish free riders with a cost, cooperators never bear the cost. In other words, cooperators “take a free ride” on punishers’ punishment of free riders, the so-called second-order free ride. Natural selection therefore favors cooperators and leads to the extinction of altruistic punishers, and then, after the extinction of the punishers, defectors finally dominate the population of cooperators.

In a context of indirect reciprocity, it has been demonstrated that cooperation can evolve through indirect reciprocity given an appro-

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Figure 1 | Effect of cost of reputation building, $c_R$, on the evolution of cooperation. Black points indicate the case without the cost of reputation building; red represents the case with the cost (triangles: $c_R = 0.1$; squares: $c_R = 0.01$; these symbols overlap). The frequency of cooperation at the 1,000th generation is plotted as a function of cost of cooperation, $\tau$ (benefit of cooperation, $b$, is fixed at 1; population size $n = 200$; probability of implementation error $\varepsilon = 0.05$; mutation rate $\mu = 0.01$; an individual’s strategy at the first generation is determined randomly). Each point denotes the values averaged over 200 computer simulation runs. (A) Individuals use the moral assessment rule, SCORING. Top row: the average number of rounds for each individual in a generation, $m$, is 3; Middle row: $m = 5$; Bottom row: $m = 7$. (B) MILD. (C) STERM.
indirect reciprocity. One candidate is multilevel (group) selection. Suppose that individuals of a population are subdivided into groups and interact within these groups, and that individuals who build reputations are concentrated together within the same groups. Then, groups of individuals who build reputations can achieve high-level indirectly reciprocal cooperation and thus, despite the cost of reputation building, outperform the other groups of individuals who do not build reputations. Consistent with this conjecture, it has been demonstrated that, in the absence of costs of reputation building, multilevel selection supports the evolution of a moral assessment rule under which indirectly reciprocal cooperation is evolutionarily stable.

Another candidate is network reciprocity. In a typical setting considered in studies of network reciprocity, individuals of a population occupy the vertices of a graph and the edges determine who interacts with whom. That is, each individual plays a game only with her neighbors and mimics the most successful neighbor’s strategy. In this setting, individuals who build reputations can form a cluster in which indirect reciprocity is established, and thus might be able to prevail in the population.

Moreover, it might be possible that building reputations is beneficial enough to overcome the cost in situations that differ from those considered in our study. Indeed it has been mathematically shown that, when individuals engage in several games, an evolutionary outcome of a single game cannot be predicted without assessing the structures of the other games. How these mechanisms complement indirect reciprocity in the presence of the cost of reputation building will require further investigation.

Further, it is worth noting that indirectly reciprocal cooperation does not necessarily rely only on reputation building. For example, if the population is small enough, each individual can judge others’ goodness by direct observation, instead of the indirect observation via reputation. Moreover, experimental studies on humans and rhesus monkeys demonstrated another type of indirect reciprocity: an individual is more likely to help anonymous others when she received help in previous interactions, compared with when she did not. This type of reciprocity, called upstream indirect reciprocity, seems to be driven by a feeling of gratitude rather than reputation building. However, to date, few studies have provided theoretical explanations of the evolutionary origin of upstream indirect reciprocity.

Humans’ sociality is supported by their sophisticated cognitive abilities, e.g., language skills, which are biologically costly. Despite the importance of the cost of intelligence in human evolution, little is known about the effects of this cost on the evolution of cooperation (but see references). This study is, to our knowledge, the first to assess the relationship between the cost of high intelligence and the evolution of indirect reciprocal cooperation, highlighting the importance of considering the costs of high-level cognitive abilities in studies of the evolution of humans’ and animals’ social behavior.

**Methods**

**Reputation dynamics in the basic analytical model.** Here we show that the dynamics of the fraction of individuals among (p, q) strategists who have a good reputation, G(p, q), depends on p, but not on q.

We consider various ways to update reputations, called moral assessment rules. One way is that cooperation (defection) is simply regarded as good (bad) irrespective of the donor’s or the opponent’s reputation. Another way is to introduce the concept of justified defection: defection against a bad opponent is judged as good. Moreover, one might judge cooperation with a bad opponent as bad, which is the concept of unjustified cooperation. Taking these possibilities together, we assume that individuals in a community share the same moral assessment rule and they judge a donor’s goodness based on the donor’s own reputation and behavior and the opponent’s reputation.

A moral assessment rule is then represented by an eight-dimensional vector, R = (R_RBCG, R_RBDB, R_RCGD, R_RGDB, R_RGCB, R_RCG, R_RG), where the subscript letters indicate, from the left to the right, the donor’s reputation, the donor’s behavior and the opponent’s reputation, respectively, and R = 0, 1 denotes the probability that the donor’s behavior is judged as good in each of the eight situations. For example, (0, 0, 1, 0, 1, 0, 1, 1) indicates IMAGE SCORING in which cooperation ( defection) is simply regarded as good (bad).

At round t, consider the probabilities that: (1) a bad (p, q) strategist defects against a bad opponent, (1 − G(p, q))(1 − p_G); (2) a bad (p, q) strategist defects against a good opponent, (1 − G(p, q))(1 − p_G); (3) a bad (p, q) strategist cooperates with a bad opponent, (1 − G(p, q))p_G; (4) a bad (p, q) strategist cooperates with a good opponent, (1 − G(p, q))p_G; (5) a good (p, q) strategist defects against a bad opponent, G(p, q)(1 − p_G)(1 − G); (6) a good (p, q) strategist defects against a good opponent, G(p, q)(1 − p_G)G; (7) a good (p, q) strategist cooperates with a bad opponent, G(p, q)p_G(1 − G); and (8) a good (p, q) strategist cooperates with a good opponent, G(p, q)p_G. These probabilities are represented by a vector, S. Since each component of S is a function of G(p, q) and p, we rewrite S as S(G(p, q), p).

Recall that the reputation of a unit individual is updated only when the observer decides to build that individual’s reputation, the probability of which is given by Eq. (3).

**Extended analytical model.** Here we assume that each individual makes decisions based not only on the opponent’s reputation but also on his/her own reputation. In this case, a behavioral strategy is denoted by a four-dimensional vector, p = (p_RBCG, p_RBDB, p_RCGD, p_RGDB), where the left subscript letter denotes the focal individual’s own reputation, the right denotes the opponent’s reputation, and p represents the probability that s/he cooperates given his/her own reputation and that of the opponent. Here, the average payoff of (p, q) strategists at round t can be calculated as:

\[
\pi_t((p, q)) = \frac{1}{b} \left( p \cdot (R(p, q)B(p, q)G(p, q)R(p, q)G(p, q)G(p, q)R(p, q)G(p, q)) + G(p, q)p_G(G(p, q)G(p, q)p_G) \right) - \text{cost}.
\]

**Conclusion.** The evolutionary dynamics of indirect reciprocity are robust to changes in the model and to variations in the data. However, the role of the cost of reputation building and the effects of this cost on the evolution of cooperation and sociality in humans and animals remain to be explored.
9. Ohtsuki, H. & Iwasa, Y. Global analyses of evolutionary dynamics and exhaustive search for social norms that maintain cooperation by reputation. *J Theor Biol* **244**, 518–531 (2007).
10. Suzuki, S. & Akiyama, E. Evolution of indirect reciprocity in groups of various sizes and comparison with direct reciprocity. *J Theor Biol* **245**, 539–552 (2007).
11. Sigmund, K. Moral assessment in indirect reciprocity. *J Theor Biol* **299**, 25–30 (2012).
12. Brosnan, S. F., Salwiczek, L. & Bshary, R. The interplay of cognition and cooperation. *Philosophical Transactions of the Royal Society B: Biological Sciences* **365**, 2699–2710 (2010).
13. McNally, L., Brown, S. P. & Jackson, A. L. Cooperation and the evolution of intelligence. *Proceedings of the Royal Society B: Biological Sciences* **279**, 3027–3034 (2012).
14. Ohtsuki, H. & Iwasa, Y. How should we define goodness? – reputation dynamics in indirect reciprocity. *J Theor Biol* **231**, 107–120 (2004).
15. Takahashi, N. & Mashima, R. The importance of subjectivity in perceptual errors on the emergence of indirect reciprocity. *J Theor Biol* **243**, 418–436 (2006).
16. Panchanathan, K. & Boyd, R. A tale of two defectors: the importance of standing for evolution of indirect reciprocity. *J Theor Biol* **224**, 115–126 (2003).
17. Brandt, H. & Sigmund, K. The good, the bad and the discriminator – errors in direct and indirect reciprocity. *J Theor Biol* **239**, 183–194 (2006).
18. Brandt, H. & Sigmund, K. The logic of reprobation: assessment and action rules for indirect reciprocation. *J Theor Biol* **231**, 475–486 (2004).
19. Fishman, M. A. Indirect reciprocity among imperfect individuals. *J Theor Biol* **225**, 285–292 (2003).
20. Leimar, O. & Hammerstein, P. Evolution of cooperation through indirect reciprocity. *Proc Biol Sci* **268**, 745–753 (2001).
21. Pacheco, J. M., Santos, F. C. & Chalub, F. A. C. C. Stern-judging: A simple, successful norm which promotes cooperation under indirect reciprocity. *PLoS Comput Biol* **2**, e178 (2006).
22. Suzuki, S. & Akiyama, E. Reputation and the evolution of cooperation in sizable groups. *Proc Biol Sci* **272**, 1373–1377 (2005).
23. Tanabe, S., Suzuki, H. & Masuda, N. Indirect reciprocity with trinary reputations. *J Theor Biol* **243**, 475–488 (2006).
24. Fehr, E. Human behaviour: don’t lose your reputation. *Nature* **432**, 449–450 (2004).
25. Panchanathan, K. & Boyd, R. Indirect reciprocity can stabilize cooperation without the second-order free rider problem. *Nature* **432**, 499–502 (2004).
26. Boyd, R., Gintis, H., Bowles, S. & Richerson, P. J. The evolution of altruistic punishment. *Proc Natl Acad Sci USA* **100**, 3531–3535 (2003).
27. Hauert, C., Traulsen, A., Brandt, H., Nowak, M. A. & Sigmund, K. Via freedom to coercion: the emergence of costly punishment. *Science* **316**, 1905–1907 (2007).
28. Nakamaru, M. & Iwasa, Y. The coevolution of altruism and punishment: role of the selfish punisher. *J Theor Biol* **240**, 475–488 (2006).
29. Traulsen, A. & Nowak, M. A. Evolution of cooperation by multilevel selection. *Proc Natl Acad Sci USA* **103**, 10952–10955 (2006).
30. Boyd, R. & Richerson, P. J. Group beneficial norms can spread rapidly in a structured population. *J Theor Biol* **215**, 287–296 (2002).
31. Bowles, S., Choi, J.-K. & Hopfensitz, A. The co-evolution of individual behaviors and social institutions. *J Theor Biol* **223**, 135–147 (2003).
32. Ohtsuki, H., Hauert, C., Lieberman, E. & Nowak, M. A. A simple rule for the evolution of cooperation on graphs and social networks. *Nature* **441**, 502–505 (2006).
33. Santos, F. C., Pacheco, J. M. & Lenaerts, T. Evolutionary dynamics of social dilemmas in structured heterogeneous populations. *Proc Natl Acad Sci USA* **103**, 3490–3494 (2006).
34. Hashimoto, K. Unpredictability induced by unfocused games in evolutionary game dynamics. *J Theor Biol* **241**, 669–675 (2006).
35. Greiner, B. & Vittoria Levati, M. Indirect reciprocity in cyclical networks. *Journal of Economic Psychology* **26**, 711–731 (2005).
36. Stanca, L. Measuring indirect reciprocity: Whose back do we scratch? *Journal of Economic Psychology* **30**, 190–202 (2009).
37. Rutte, C. & Taborsky, M. Generalized reciprocity in rats. *PLoS Biol* **5**, e196 (2007).
38. Pfeiffer, T., Rutte, C., Killingback, T., Taborsky, M. & Bonhoeffer, S. Evolution of cooperation by generalized reciprocity. *Proc Biol Sci* **272**, 1115–1120 (2005).
39. Nowak, M. A. & Roch, S. Upstream reciprocity and the evolution of gratitude. *Proc Biol Sci* **274**, 605–609 (2007).
40. Iwagami, A. & Masuda, N. Upstream reciprocity in heterogeneous networks. *J Theor Biol* **265**, 297–305 (2010).
41. Binmore, K. & Samuelson, L. Evolutionary stability in repeated games played by finite automata. *Journal of Economic Theory* (1992).
42. Imhof, L., Fudenberg, D. & Nowak, M. Evolutionary cycles of cooperation and defection. *Proc Natl Acad Sci USA* **102**, 10797 (2005).
43. Nowak, M. & Sigmund, K. The dynamics of indirect reciprocity. *J Theor Biol* **194**, 561–574 (1998).

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S.S. and H.K. designed and performed the research; S.S. wrote the paper.

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