Evaluation of information retrieval systems using structural equation modeling

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Evaluation of Information Retrieval Systems
Using Structural Equation Modelling

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Abstract

The interpretation of the experimental data collected by testing systems across input datasets and model parameters is of strategic importance for system design and implementation. In particular, finding relationships between variables and detecting the latent variables affecting retrieval performance can provide designers, engineers, and experimenters with useful if not necessary information about how a system is performing. This paper discusses the use of Structural Equation Modelling (SEM) in providing an in-depth explanation of evaluation results and an explanation of failures and successes of a system; in particular, we focus on the case of evaluation of Information Retrieval systems.
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1 Introduction

Humans often have to find solutions to problems. The attempts to find solutions are the main causes of information needs. To meet information needs, users search for relevant information while avoiding useless ones. The aforementioned context is where Information Retrieval (IR) systems perform the complex of activities to represent and retrieve documents containing information relevant to user’s information needs, thus becoming a crucial function of computerized information systems.

Effective retrieval systems should be designed to obtain high precision\(^1\) and high recall\(^2\). To obtain a measure of retrieval effectiveness, designers and experimenters employ a variety of test collections, since the effectiveness of a retrieval system may widely vary according to queries and retrieval algorithms; for example, Harman and Buckley [2009] report that large variations in measures of effectiveness may be observed for Relevance Feedback (RF) when varying the number of feedback documents and terms.

Understanding the reasons of retrieval failures and measuring the room for effectiveness improvement is of strategic importance for system design and implementation. The interpretation of the experimental data collected by testing retrieval systems across variables would help designers and researchers to explain whether and when a system or a component thereof performed better or not than another system or component.

Despite the unquestionable importance of in-depth analysis of experimental results, many research papers fail to provide insights into experiments, apart from some statistical significance tests which, however, rarely point out retrieval model weaknesses. One reason for the lack of methodologies supporting researchers and experimenters in interpreting the retrieval failures is the absence of a language that can help communicate in spoken or written words, variables and causal relationships thereof.

The principal purpose of this paper is thus to explain how to fill the gap between a mere – even though necessary – description of tables, graphs and statistical testing, on the one hand, and the use of advanced statistical methods to describe the variables and their relationships that characterise retrieval performance in a more natural way than traditional statistics. We argue that Structural Equation Modelling (SEM) can be such a methodology.

The paper is structured as follows. Section 2 describes the context of the paper and mentions some relevant related work. Section 3 remarks on the use of SEM in IR and explains the main differences among analysis methods. In Section 4, we explain how SEM can be applied to IR by means of a series of experimental case studies. Section 5 comments on the potentiality of SEM in IR.

\(^1\)The proportion of retrieved documents that are found relevant.

\(^2\)The proportion of relevant documents that are retrieved.
2 Related Work

SEM is a general methodology encompassing multivariate methods addressed in IR since Salton [1979]’s research work; other notable examples include Deerwester et al. [1990]’s Latent Semantic Analysis (LSA) and other Factor Analysis (FA) methods utilized in contextual search [Melucci, 2012].

The IR community has already developed some approaches to analyzing the causes of both missing relevant documents and the retrieval of irrelevant documents; reliability analysis, retrievability analysis, query performance prediction and axiomatic analysis are the most utilized to this end. Some approaches might have been missed, however, those mentioned are the principal approaches in our opinion and to our knowledge.

2.1 Reliability, Retrievability, Query Performance Prediction and Rank Correlation

2.1.1 Reliability

Reliability is concerned with situations where a system retrieves relevant documents and misses non-relevant documents across a set of queries. A major factor in the unreliability of a system is the extremely large variation in performance across queries. When different systems or variants are considered, variation can also be caused by system algorithms and implementations.

A systematic approach to understanding the reasons why systems fail in retrieving relevant documents or succeed in retrieving irrelevant documents has been implemented by the Reliable Information Access (RIA) workshop documented by Harman and Buckley [2009]. We summarise the main outcomes as follows:

- although systems tend to retrieve different document sets, they tend to fail for the same reason, i.e. wrong query understanding due to, for example, over/under stemming or missed synonyms;
- systems not only tend to emphasize the same query aspects, but they also emphasize wrong aspects;
- Buckley [2009] reported that variations in system performance can occur
  - across queries in terms of Average Precision (AP), thus calling for an analysis at the level of query, and
  - across systems or variants thereof, e.g. particular devices such as relevance feedback or query expansion;
- most of the average increase of effectiveness of query expansion is due to a few queries that are greatly improved;
• performance is increased by several good terms and cannot be increased by one single crucial term;

• along these lines, Ogilvie et al. [2009] suggested cross-validation to find the best number of terms.

Approaches inspired to data mining to understanding retrieval failures were also proposed by Bigot et al. [2011]. Reliability analysis also investigated the best practices for learning to rank deployments by Macdonald et al. [2013]. The analysis reported was performed starting from a series of research hypotheses about the impact of sample size, type of information need, document representation, learning to rank technique, evaluation measure, and rank cutoff of the evaluation measure on the observed effectiveness. The methodology that was implemented by Macdonald et al. [2013] to perform the analysis was based on the definition of some variables and three research themes, i.e. sample size, learning measure and cutoff; the research themes were associated to the variables, which were labeled as either fixed or factor. Sample size definition was also addressed by Voorhees and Buckley [2002] using empirical error rates, as well as by Sakai [2014] using power analysis, paired t-test, and Analysis of Variance (ANOVA). Moreover, Bailey et al. [2015] also reported that the system performance variations of a single system across queries is comparable or greater than the variation across systems for a single query.

2.1.2 Retrievability

Retrievability concerns the variations between systems with respect to the rank of the same retrieved document, according to Azzopardi and Vinay [2008]. Retrievability may also depend on the subsystems (e.g. crawlers) that decide which documents are indexed, the way users formulate queries, the retrieval functions, the user’s willingness to browse document lists, and the system’s user interface. Many systems make many documents little retrievable and rank documents in lists that would not change were little retrievable documents removed from the index. A measure of retrievability of document \( d \) was proposed by Azzopardi and Vinay [2008]:

\[
ret(d) = \sum_{q \in Q} L(q) f(r(d,q), r^*)
\]

where \( Q \) is set of queries, \( r(d,q) \) is the rank of \( d \) in the retrieved document list, \( L(q) \) is the likelihood of \( q \), \( r^* \) is the maximum examined document rank, and \( f \) is the cost/utility of \( d \). The computation of \( ret(d) \) is challenging since it should be estimated across many different systems and many different queries. Low retrievability causes retrieval bias since a system may favor the most retrievable documents. Wilkie and Azzopardi [2014] reported that a negative correlation exists between retrieval bias and some retrieval performance measures, thus suggesting that reducing retrieval bias would increase performance.
2.1.3 Query Performance Prediction

Query Performance Prediction (QPP) deals with situations where a specific query fails or succeeds in retrieving relevant documents, whereas retrievability analysis is only based on using document features and reliability analysis is based on query sets. A measure of query ambiguity and then of a QPP called query clarity was proposed by Cronen-Townsend et al. [2002] and further improved and extended by Hauff et al. [2008]. The intuition behind query clarity is that, the more different the query language from the collection language, the less the ambiguity and then the better the retrieval performance. The clarity score of a query is the Kullback-Liebler Divergence (KLD) between the collection language and the query language. The query language is estimated by the set of retrieved documents matching the query. The more diverse the latter and the more similar it is to the collection language, the more the query is ambiguous. QPP usually estimates effectiveness without relevance judgments, but using retrieved document features. However, assessing very few top-ranked documents can dramatically improve QPP quality according to Butman et al. [2013]. Zhao et al. [2008], Zhou and Croft [2006] proposed further measures and techniques. Moreover, Hauff et al. [2010] found that the user’s predictions of query performance do not correlate with the system’s predictions; on the other hand, different approaches were described by Kurland et al. [2012] in one uniform framework; association rules were applied to the discovery of poorly performing queries by Kim et al. [2013]; and some explanations of why QPP might not work as expected were reported by Raiber and Kurland [2014]. Cummins [2014] proposed to predict query performance from document score distributions and also provides a good and up-to-date survey of QPP.

2.1.4 Rank Correlation

An alternative approach to comparing runs might be based on rank correlation measurement. Rank correlation refers to a family of statistical measures of the degree to which two rankings should be considered similar, that is, the items of a ranking are disposed approximately in the same order as the same items in another ranking; examples of rank correlation measures are the $\tau$ coefficient by Kendall [1938] and the $\rho$ coefficient by Spearman [1904].

The main advantage of rank correlation measures is the simplicity of measuring the degree to which two rankings are similar using one single number, which may be tested for significance because it can often be provided with a probability distribution under the null hypothesis of null correlation when samples are large enough.

The main weakness of rank correlation measures is the poor description capability, because these measures are unable to distinguish between exogenous variables and endogenous variables and between latent and manifest variables. A rank correlation measure is a zero-dimensional measure whereas a structural equation model is a multidimensional measure; for example, if Kendall’s tau of the correlation between two
measures of effectiveness may be statistically significant, but if the value is small, the coefficient is little informative about the differences between the tested systems.

2.1.5 Comparison to SEM

Retrievability, query ambiguity and QPP are related each other. Retrievability depends on query ambiguity, since an ambiguous query is more likely to select less relevant documents than an unambiguous query. Moreover, QPP is obviously related to query ambiguity. Incorporating user variability in system-based evaluation is also somehow related to QPP. User variability allows the researchers to more precisely measure the effectiveness of the system to different segments of the user base, thus allowing them to predict which systems will be the most effective in performing a certain user’s task; see the papers by Carterette et al. (2011, 2012).

Reliability analysis, retrievability analysis, and QPP are performed with the idea that a retrieval system can be viewed as a black box in which independent variables can be entered and dependent variables can be observed. Following this idea, the variations of the latter can be explained by the variations of the former.

A quite different approach to understanding retrieval failures and successes – it might be named axiomatic – was suggested by Fang et al. [2004] and Fang and Zhai [2005]. The basic idea of the axiomatic approach is that (1) some heuristic rules can be defined to describe an effective retrieval function and (2) the inefficacy of a retrieval function is related to the retrieval function’s failure to comply with these heuristic rules in the sense that the rules are necessary conditions of effective retrieval, that is, the violation of a rule determines a loss of effectiveness. The potential of the axiomatic approach can be exploited to improve the retrieval functions violating the rules as reported by Fang et al. [2011].

On the one hand, reliability analysis, retrievability analysis, and QPP are specific to IR. On the other hand, SEM was investigated and applied to complex social, economic, and psychological phenomena. For example, attitudes, personality traits, health status, and political trends are often variables of interest to sociologists. Intellectual abilities of students or teaching styles of instructors are important variables in education. The relationship between demand and supply is very important to economists; some examples are reported in Section 2.4.

2.2 Structural Equation Modelling in Interactive Information Retrieval

SEM is still in its infancy within laboratory-based IR; in contrast, it recently received a great deal of attention in Interactive Information Retrieval (IIR) because it provides an effective framework to modeling the complex variables emerging from the interaction between user and IR system. The theme of interaction between user and system was at the root of IR since the early Eighties when Belkin et al. [1982a,b] addressed the
problem of the Anomalous States of Knowledge (ASK) as well as Marchionini and Shneiderman [1988] and Marchionini and Crane [1994] investigated how hypertext systems can induce a novel approach to searching for information.

The occurrence of latent factors in the user’s mind such as search task and intent and the inherent difficulty in measuring these factors were the main reasons why quantitative methods measuring latent factors by means of manifest variables were suggested to assess the importance and the relationships among variables and factors; to this respect, SEM represents the most general framework. Therefore, in IIR, SEM has been drawing attention to a degree that some tutorials such that that presented by Kattenbeck and Elsweiler [2018] are becoming necessary or useful for systematizing the corpora of research articles such as those authored by Zhang et al. [2014] and Ishita et al. [2017].

In this paper, we limit ourselves to the use of SEM in laboratory-based IR evaluation, which has received a little deal of attention, without further addressing the already covered use in IIR.

2.3 Comparison to Other Approaches to Analyzing Experimental Data

The statistical inference performed using experimental data provides some guidance to see whether two systems performed to a similar degree; for example, it helps decide whether the average difference in precision between system (or component) performances is due to chance or it signals a diversity between the systems (or components). A statistical estimator measures the difference; the p-value of the estimator can measure the statistical significance of the estimated value, that is, the degree to which the difference should not be considered a random fluctuation. This approach to evaluating systems is indeed the standard practice of evaluation as reported by many research papers.

Other questions about the reasons that a system or component performed better or worse than another system or component would require further statistical methodologies which are sadly less frequently reported in the literature on evaluation. Indeed, an inferential analysis whether a system performed differently from another is unable to explain retrieval performance variations. A consequence of the lack of explanation of the differences in performance between systems is the difficulty in improving retrieval performance – the retrieval performance observed for some queries can be improved when the reasons that make the retrieval system ineffective become known to the researchers.

SEM may support researchers because it provides them with a language to describe observed data. The opportunity – and the necessity – of choosing an appropriate

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3The p-value of a difference is the probability of measuring a value greater than the absolute value of the observation when the true difference is zero (null hypothesis). The p-value is then an indirect way to measure how far the observation is from the null hypothesis.
Table 1: For each column and row, 'Y' means that an analysis method (column) owns a property (row). Association means that two variables increase or decrease together; pure association means that association depends only on $X$ and $Y$, otherwise association is spurious. Directionality means that a variable can be either exogenous or endogenous, and the influence of $X$ on $Y$ differs from the influence of $Y$ on $X$. Prediction means that some independent variables determine, i.e., predict, some dependent variables. Heterogeneity means that some variables can be both exogenous and endogenous. Latent variables means that experimenters can define latent variables. Latent association means that experimenters can define association between latent variables. Causality means that experimenters can test whether the hypothesis that one variable depends on another variable is confirmed by the observed data.

A model is toward stimulating and helping researchers to explain their experimental results beyond a mere—even though necessary—textual description of tables, graphs and statistical testing. The dependency on the experimenter’s knowledge of the domain to which the process is applied (e.g., IR experimentation) is a strength, since it makes the experimenter’s point of view explicit and reproducible.

SEM can be viewed as generalization of other multivariate analysis. In this section we provide a comparison to help readers to understand the SEM advantages. To this end, we prepared Table 1.

Association is owned by every analysis method because correlation is at the basis of more complex analysis. If only correlation matrices are used, correlation analysis cannot in its own distinguish the direction of association. Heterogeneity cannot even more so be distinguished because covariance is commutative. If there are three or more variables, pure association can be measured using correlation, however, the semantics of purity would make sense only if directionality held. Heterogeneity would imply that some variables determine other variables and therefore that directionality holds. Correlation between latent variables—and association thereof—can only be estimated by manifest variables.

Regression extends correlation in that variables can be either exogenous or endogenous because of directionality. (Regression coefficients are not commutative.) Regression detects pure association, since beta coefficients can be calculated between variable pairs without the influence of third variables. Path analysis can be represented
by – or is a specialization of – regression, since a variable can be both endogenous (i.e. predicted) and exogenous. Indeed, heterogeneity implies directionality.

Factor Analysis (FA) allows experimenters to extract latent factors from observed data. FA can be either exploratory – the number of factors is unknown – or confirmatory – mainly concerned with testing hypotheses about the number of factors and the significance of the relationships between factors and manifest variables.

The basic difference from SEM is mainly concerned with estimating relationships between latent variables, i.e. factors, whereas confirmatory factor analysis is mainly concerned with the degree to which a factor determines a manifest variable. Confirmatory factor analysis does not model association between latent variables as SEM does.

As for causality, it must be understood that SEM does not discover causal relationships between variables. Bollen and Pearl [2013] stated that “researchers do not derive causal relations from a [structural equation model]. Rather the [structural equation model] incorporates the causal assumptions of the researcher. These assumptions derive from the research design, prior studies, scientific knowledge, logical arguments, temporal priorities, and other evidence that the researcher can marshal in support of them. The credibility of the [structural equation model] depends on the credibility of the causal assumptions in each application.” What SEM can do is to test the consistency between data and causal relationships assumed by researchers.

Multilevel Modeling (MLM) groups data into larger clusters so that scores within each cluster may not be independent. Recently, Crescenzi et al. [2016] have investigated MLM to evaluate a number of hypotheses about the effects of time constraint, system delays and user experience. MLM and SEM might converge to a single framework according to Kline [2015] and Bartholomew et al. [2008].

In contrast to SEM, stepwise regression selects the best predictors based on statistical significance (i.e. p-value). In practice, the predictor showing the lowest p-value of its regression coefficient is selected and added to the model. After the addition of the best predictor, the worst predictors showing the highest p-values or the p-values above a threshold are removed from the model. Although a stepwise regression function may compute the best model in a short time, automatic predictor selection may depend on the solution of the actual sample utilized to fit the model while another sample might suggest another model [Kline, 2015].

2.4 Structural Equation Modelling and Other Domains

In addition to the investigation of socio-economic phenomena, some uses of SEM regarded research areas that are somehow relevant to IR, since the factors affecting users’ access to information systems were investigated. SEM was utilized by Chan et al. [2005] to examine the multiple causal relationships among the performances for different tasks (modeling, query writing, query comprehension) performed by the users of a database interface, in which the data model and query language are major compo-
A structural equation model was also used to investigate users’ behaviour within community networks by Kwon and Onwuegbuzie [2005], Bulletin Board Systems by Chen and Chiu [2007], Wikipedia by Cho et al. [2010], social network systems by Kipp and Joo [2010] and Park [2014], electronic commerce by Lu and Zhu [2010] and Afzal [2013], library systems by Sin [2010], exploratory search by O’Brien and Toms [2013], agile software development by Senapathi and Srinivasan [2014], and online education by Zhang and Dang [2015]. Kher et al. [2009] used a variation of SEM called Latent Growth Modeling to study longitudinal data where time is a relevant variable.

3 Remarks on the Use of Structural Equation Modelling

The basic idea underlying the use of SEM in IR is that the evaluation of indexing and retrieval of large and heterogeneous document collections performed by an IR system may be viewed as a phenomenon similar to the social and economic phenomena investigated by SEM. According to this view, an investigator is supposed to be unable to explain all the reasons why a system failed or succeeded in performing indexing and retrieval operations, since the complexity of the document collections and of the user’s queries can be at the level that goes beyond the potential of the investigator’s instruments. The complexity might not be caused by the retrieval system’s software architecture – it can be well known and documented – rather, it may be due to the heterogeneity of the document collection and the context-sensitiveness of the user’s interaction and relevance assessment.

However complex the evaluation of indexing and retrieval of large and heterogeneous document collections may be, our rationale is that IR evaluation results can be described by causal hypotheses between variables using SEM, where the variables are both latent or manifest quantities that are taken as input while regression coefficients, beta coefficients and fit indexes are given as output.

This section illustrates the main properties that make SEM suitable for IR experimental results investigation. In summary, we will explain the following reasons: experiments consists of observing manifest variables; covariation (e.g. between relevance assessments and frequency) is at the basis of experimental analysis; association between variables are often directed; latent variables (e.g. eliteness) are integrated with manifest variables (e.g. frequency); experimenters may investigate whether some variables (e.g. frequency or eliteness) cause a change in other variables (e.g. relevance). In the following, these properties are discussed.

“[G]eographically based Internet services that provide local residents a full range of Internet services and other information and communication technology related services, including computer and Internet training, setting up public access sites, the creation of digitized local information database, and organisational ICT consulting.” [Kwon and Onwuegbuzie, 2005]
3.1 Variables and Covariation

IR is naturally based on variables since the researchers can only come to an understanding of how users and systems interact by using variables. The variables measured in IR can be qualitative (e.g. class membership), quantitative (e.g. term frequency), ordinal (e.g. document rank), cardinal (e.g. document set size), integer or real. Moreover, the variables are often random, since some indexing and retrieval processes (e.g. relevance assessment) are subject to uncertainty. In addition, covariation is the basis for many retrieval and indexing models not only for finding term or document correlations, but also for estimating the conditional probabilities that are necessary for term weighting schemes such as Best Match N. 25 (BM25).

The SEM’s output provides evidence about whether the causal hypotheses of a structural equation model such as \( X \rightarrow Y \) can be confirmed by the data collected from the manifest variables; for example, if the causal hypotheses of a structural equation model are made between a variable measuring retrieval effectiveness, \( Y \), and variables describing the indexing and retrieval processes dictated by a retrieval model, \( X \), the SEM’s output provides evidence about whether \( X \) can explain \( Y \) and it may indicate some reasons that a retrieval system performed badly (low \( Y \)) or satisfactorily (high \( Y \)) by associating the values of \( X \) to the values of \( Y \).

Although covariation cannot be considered sufficient for convincing someone of a causal relationship between two variables, it is nevertheless necessary in IR since it is unlikely that a causal relationship between two variables (e.g. term frequency and pertinence) will occur without covariation. The direction of the relationship between variables implies the distinction between exogenous variables and endogenous variables as explained in the next section.

3.2 Endogenous Variables and Exogenous Variables

In general, endogenous variables are quite well distinguished from exogenous variables in IR. The distinction between exogenous and endogenous variables is made easier since it is possible to assign the role of exogenous variables to features of documents and queries and the role of endogenous variables to relevance assessments and retrieval effectiveness measures, for example. Exogenous manifest variables are usually frequencies, probabilities or sizes observed from the collection indexes and aggregated at the level of topic or document; for example, a variety of document statistics can be observed for each document and then associated to its rank in a list of retrieved documents. When evaluation in IR is considered, endogenous variables are usually referred to measures of user satisfaction or document relevance; for example, retrieved document rank is an endogenous manifest variable observed at the level of document and AP or Normalized Discounted Cumulative Gain (NDCG) are endogenous manifest variables observed at the level of topic. In this way, the variations of precision and recall can be explained by the variations of exogenous or other endogenous variables.
Once endogenous variables and exogenous variables are assigned, an explanation of the reasons why a system performs better than another system can be suggested in terms of differences in the ways the exogenous variables are implemented by the systems being compared. A richer description of the relationships between variables can be obtained if additional factors explaining the reasons why the exogenous variables may vary are added; for example, in interactive IR, query expansion devices, relevance feedback algorithms and other methods implementing user-document interaction may be considered as exogenous variables, while measures other than precision such as user satisfaction or document utility may integrate the endogenous variables; in Information Seeking, typical endogenous variables have been the frequency of information sources used in various groups [Vakkari and Järvelin, 2005].

### 3.3 Latent Variables and Manifest Variables

While many variables, such as frequencies, are manifested because they can be obtained by counting, other variables such as relevance and eliteness should be viewed as latent. Relevance can be viewed as a latent variable because it results from complex intellectual activities that cannot directly be measured. However, relevance can indirectly be measured by means of manifest variables that are considered signals or indicators of relevance. Relevance labels or degrees are examples of relevance indicators because they can be collected from human assessors or users, although they cannot represent the context in which a document is deemed to be relevant.

Latent topics are another example of latent variables, since they are unobserved terms, phrases or other textual sources that can indirectly be observed in the form of (sequences of) words. LSA which aims to discover latent topics in the forms of word vectors by using unsupervised statistical methods (e.g. Singular Value Decomposition (SVD)) provides another example.

Data are usually raw in IR since they are available as frequencies, scores, and other numeric values. The problem with reproducing raw data is that experimental systems often calculate weights and scores using different parameters or methods, thus making the results slightly different. If raw data and exhaustive and precise documentation thereof were publicly available, experiments might be reproduced. Otherwise, covariance matrices are a compact alternative to raw data. When covariance matrices are available, simulation or meta-analysis can be performed, thus making experimental replication possible; for example, a researcher may make his own covariance matrices available to the research community, thus allowing the other researchers to reproduce experiments and compare the experimental results without forcing them to reproduce the experimental context and recollect the data.

The datasets used when SEM is applied to IR may store many records since IR experiments may produce large amounts of data from big test collections. For example, the datasets used in this paper (see Section 4) contain millions of documents, thousands of queries and hundreds of features for each document-query pair. When runs are
utilized, it is likely to be forced to process thousands of retrieved documents. As SEM is a large sample methodology, its application to IR does not pose a problem. Rather, some attention should be paid to the risk of easily rejecting null hypotheses because of very large samples which may make any difference significant.

The datasets mentioned above and especially the learning-to-rank datasets may contain many features selected with the idea of providing the largest possible amount of data to the researchers. In that case, some variables may be highly collinear. For example, term frequency and TFIDF might be highly collinear if the IDF component discriminates terms very little. We found a significant number of highly collinear variables in the datasets used in the experiments reported in Section 4.

In IR, descriptive analysis is often performed by the researchers and reported in the papers. For example, the variables that affect system effectiveness measured by AP are averaged and the variability across topics can be described. Descriptive analysis tells what happens, however, it cannot tell whether the variations observed are significant. Another kind of analysis can be the comparison between retrieval systems or components thereof; for example, the Mean Average Precisions (MAPs) of two competing retrieval systems can be compared and the statistical significance of the difference between the MAPs can be assessed in terms of p-value. A more complex analysis can be provided by success and failure analysis, which provides evidence as to when a system fails to retrieve relevant documents or succeeds in retrieving irrelevant documents (reliability) or as to when the system failed to retrieve documents, tout-court (retrievability).

SEM is a complex of statistical procedures that may provide an explanation of retrieval failures and successes because it allows the researcher to express some hypotheses and test whether the observed data fit the model. If these hypotheses were confirmed and if they were expressing reasons why a system performed badly or worse than another system, we would be provided with a sound methodology for diagnosis in IR evaluation. It may be used to check whether some general ideas underlying retrieval models are fitted by the data; for example, this analysis will be used in Section 4 to test whether the observed data fit the structural equation model relating a combination of authority and content to retrieval effectiveness, thus testing whether this combination can help select relevant documents; another example will be the structural equation model relating eliteness, term frequency and relevance and underlying BM25.

The measurement of latent variables and the causal effects among observed variables represent two kinds of structural equation models, i.e. Confirmatory FA (CFA) models and Path Analysis (PA) models. The experiments that are reported in this paper are about both types; however, the manifest variables are predominant in IR. The datasets of IR experiments (e.g. test collections and learning-to-rank datasets) usually include a number of manifest variables calculated from documents, queries and user actions. In particular, the endogenous variables are usually retrieval effectiveness values where the exogenous variables are collection, document, query or user features.
Many manifest variables are interrelated and one variable may result from the other; for example, the sum of TFs in titles may determine the sum of TFs in documents and different PA models may arise.

A beta coefficient is different from the correlation coefficient between two variables. Suppose $X_1$ is term frequency, $X_2$ is click frequency, and $Y$ is AP and suppose $\text{cor}(X_1, Y) = 0.40$, $\text{cor}(X_2, Y) = 0.60$ and $\text{cor}(X_1, X_2) = 0.60$. If the researcher excluded click frequency from the structural equation model describing the relationships with AP, he might conclude that term frequency ($X_1$) positively determines retrieval effectiveness and $\beta_1 = \text{cor}(X_1, Y)$. But if the researcher included click frequency and investigated the structural equation model $\{X_1 \rightarrow Y, X_2 \rightarrow Y\}$, the beta coefficient $\beta_1$ would reflect a different relationship between term frequency and AP, since

$$\beta_1 = \frac{\text{cor}(X_1, Y) - \text{cor}(X_2, Y) \cdot \text{cor}(X_1, X_2)}{1 - \text{cor}(X_1, X_2)^2} = \frac{0.40 - 0.60 \cdot 0.60}{1 - 0.60^2} = 0.06$$

which is much lower than $\text{cor}(X_1, Y)$. The reason is that the beta coefficient controls for the correlation between the other predictors, whereas the correlation coefficient does not.

Moreover, the beta coefficients differ from the regression coefficients of a structural equation model. Suppose that $Y$ is the AP of a topic and $X$ is the term frequency. When the covariance is positive, the value of $B$ would indicate the predicted increase of performance measured by AP for every additional term occurrence. In contrast, standardized coefficients would describe the effect of term frequency on performance in standard deviation units, thus discarding the original scales of $X$ and $Y$. The beta coefficients are instead necessary to compare the predictors within one structural equation model, since they have the same standardized metric; for example, $\beta_2 = (0.60 - 0.40 \cdot 0.60)/(1 - 0.60^2) = 0.56$, which is much greater than $\beta_1$ relative to the difference between $\text{cor}(X_1, Y)$ and $\text{cor}(X_2, Y)$.

### 3.4 Fitting Models and Data

When the variables that are relevant to a structural equation model are specified and those manifest are collected and prepared, different kinds of analysis can be performed. The simplest analysis is of descriptive nature, and aims to select and summarize the data using statistical moments. The kind of analysis which we are interested to in this paper is confirmatory analysis: given a structural equation model, confirmatory analysis tests whether the observed data confirm (i.e. fit) the model. Testing the structural equation model would give evidence whether the causal hypotheses of the model can be confirmed.

In SEM, model comparison is implemented by chi-square difference statistic. Chi-square is applied to nested models, i.e. one is a proper subset of the other. For nested models, Akaike Information Criterion (AIC) or Bayes Information Criterion (BIC)
measure the information loss when an experimenter would rather choose one model than choose another model.

A structural equation model can be accepted as a valid model of the observed data if there is no difference between the covariances predicted by the model and the covariance estimated by the data. When the difference is null, the fit is exact. When the difference is almost null, the fit is close. The null hypothesis represents the researcher’s hope that the structural equation model fits the data, since the correspondence between the covariances predicted by the model and the covariance estimated by the data means that the model describes the data. The rejection of the null hypothesis should imply the rejection of the structural equation model, but the chi-square test tends to reject too often as sample sizes increase, thus making the use of different fit indexes necessary. For instance, Root Mean Square Error of Approximation (RMSEA) is a fit index where a value of zero indicates the best result whereas a values less than 0.05 is considered a good fit. Besides RMSEA, approximate fit indexes such as Comparative Fit Index (CFI) [Bentler, 1990] and Tucker-Lewis Index (TLI) [Tucker and Lewis, 1973], are continuous measures of correspondence between the covariances predicted by the model and the covariance estimated by the data; they may be viewed as the degree to which the researcher’s model is better than the independence or baseline model, in particular, when the index is 1 the fit is perfect whereas a value above 0.9 signals a good fit.

3.5 Further Explanations of the Differences between SEM and other Techniques

In this section, we provide an example of comparison between techniques used to analyzing experimental data within an IR evaluation scenario. Suppose a dataset stores one record for each retrieved document with respect to a certain topic or query. Such a record contains a retrieval effectiveness measure (e.g. Precision at rank $r$ ($P@r$)) and some features (e.g. query-document term weights); the features are collected for each retrieved document to allow researchers to analyze retrieval failures of one query at a time. Alternatively, the dataset may contain one record for each retrieval effectiveness measure at the level of topic or query; the features are collected for each query to allow researchers to analyze the overall retrieval effectiveness at the level of run. Suppose the retrieval model utilized to generate the dataset promotes documents when the query term weights increase.

The dataset should be processed to make variables as normal as possible and elimi-
nate outliers and collinearity. Then, a correlation matrix can be computed, for example:

\[
\begin{matrix}
Y & X_1 & X_2 & X_3 & X_4 & X_5 & X_6 \\
1.0 & 0.2 & 0.3 & 0.1 & -0.1 & 0.2 & 0.5 \\
0.2 & 1.0 & 0.9 & 0.1 & 0.0 & 0.0 & 0.0 \\
0.3 & 0.9 & 1.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
0.1 & 0.1 & 0.0 & 1.0 & 0.0 & 0.0 & 0.0 \\
-0.1 & 0.0 & 0.0 & 0.0 & 1.0 & 0.4 & 0.1 \\
0.2 & 0.0 & 0.0 & 0.0 & 0.4 & 1.0 & 0.9 \\
0.5 & 0.0 & 0.0 & 0.0 & 0.1 & 0.9 & 1.0 \\
\end{matrix}
\]

where \( Y \) is a retrieval effectiveness measure and the \( X_i \)'s are the retrieved document features. The correlation matrix would help experimenters to view the features that contribute more to retrieval effectiveness than others; for example, \( X_4 \) is negatively correlated with \( Y \), thus suggesting that the corresponding feature makes retrieval effectiveness worse when the feature weight increases. Actually, a correlation coefficient may hide the true relationship between \( Y \) and a feature. The beta coefficient, which is the change in standard deviations of \( Y \), given a 1-point change in standard deviation of \( X_4 \), is about equal to 0.53. The contrast between the \( X_4 \)'s beta coefficient and correlation coefficient is due to the correlation between \( X_4 \) and \( X_5 \) and to that between \( X_5 \) and \( Y \). In sum, beta coefficients reveal the true impact of features on retrieval effectiveness.

Suppose the information about the \( X \)'s correlations is unavailable or correlation is null. Beta coefficients are equal to the corresponding correlation coefficients – and they can be of little help – when the \( X_i \)'s are uncorrelated. Consider the following correlation matrix, for example:

\[
\begin{matrix}
Y & X_1 & X_2 & X_3 & X_4 & X_5 & X_6 \\
1.0 & 0.2 & 0.3 & 0.1 & -0.1 & 0.2 & 0.5 \\
0.2 & 1.0 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
0.3 & 0.0 & 1.0 & 0.0 & 0.0 & 0.0 & 0.0 \\
0.1 & 0.0 & 0.0 & 1.0 & 0.0 & 0.0 & 0.0 \\
-0.1 & 0.0 & 0.0 & 0.0 & 1.0 & 0.0 & 0.0 \\
0.2 & 0.0 & 0.0 & 0.0 & 0.0 & 1.0 & 0.0 \\
0.5 & 0.0 & 0.0 & 0.0 & 0.0 & 0.0 & 1.0 \\
\end{matrix}
\]

Experimenters might be perplexed by the negative correlation between \( Y \) and \( X_4 \); if the feature was added to the model following the idea that an increase of \( X_4 \) should cause an increase of \( Y \). Since the features are uncorrelated, an explanation cannot be given in terms of the difference between beta coefficients and correlation coefficients. SEM may provide an explanation. To obtain the explanation, the experimenters have to define a structural equation model relating the features to some latent variables, which
may explain the negative correlation with retrieval effectiveness. For example, suppose an experimenter knows that $X_5$ and $X_6$ correspond to two query term weights of the same type (e.g. two query term IDFs) and s/he suspects that one term is about a query facet complementary to the query facet of the other term. A latent variable $A$ may govern both features and cause the negative correlation. The structural equation model for this hypothesis can be written as follows:

$$ Y \leftarrow X_1 + X_2 + X_3 + X_4 + A \quad A \rightarrow X_5 + X_6 $$

However, the true nature of $A$ remains unknown; it may refer to one term or to a set of terms. Discovering how latent variables can be implemented is matter of future research.

As also explained in Section 2.3, SEM differs from other data analysis methods such as Exploratory FA (EFA). EFA computes some factors which are an alternative vector basis to the canonical vector basis underlying the observed data. The main advantage of EFA is the reduction of a large set of variables to a small set of factors which approximate the correlation matrix and then the relationships between variables. Consider the correlation matrix above. The following factors can explain 73% of variance:

$$
\begin{array}{ccc}
Z_1 & Z_2 & Z_3 \\
0.274 & 0.204 & 0.705 \\
0.896 & & 1.002 \\
& -0.183 & 0.170 \\
0.274 & 0.134 & -0.711 \\
0.984 & & -0.223 \\
0.972 & & 0.222 \\
\end{array}
$$

The numbers are a measure of the contribution of a factor to a variable and are called factor loadings. EFA indicates that $Z_1$ influences $X_5$ and $X_6$, $Z_2$ affects $X_1$ and $X_2$, and $Z_3$ influences $Y$ and $X_4$. Clearly, the factors correspond to the main subsets of related variables, yet their meaning is obscure, since $Y$ has been considered in the same way as the $X$’s although the latter have been considered exogenous variables in the structural equation model above. However, the factors that are computed from a correlation matrix cannot tell anything about the latent nature of unobserved variables. Although the factor loadings may suggest that, say, $Z_3$ is a “combination” of $Y$ and $X_4$, which was found through a covariance matrix approximation algorithm, it would be difficult to conclude that it might be viewed as a meaningful variable. Clearly, the researcher’s intervention would be necessary in the event that an interpretation were useful.
4 Using Structural Equation Modelling in Information Retrieval Evaluation

In this section, we illustrate some applications of SEM in IR evaluation. In particular, we focused on the comparison between retrieval systems and on the latent variables that make retrieval effectiveness different; for example, many retrieval systems fail in answering difficult queries – those for which precision is very low – and experimenters need to know the causes of failure. However, what makes a query difficult might not make another query difficult; therefore, two queries may require two different structural equation models. Although the structural equation models resulting from such analysis are not the same, they can suggest some insights to the experimenter about how the retrieval model should be modified in order to address the difficulty of the queries.

Some datasets are needed for calculating the actual values of the manifest variables. The data used for this paper were derived by learning-to-rank datasets and experimental retrieval results known as runs; a run is a data file storing the documents that are retrieved against each query and that are ranked according to the degree of relevance. In this paper, runs are joined with relevance assessments (qrels) to compute retrieval effectiveness measures. Learning-to-rank datasets describe documents and queries in terms of numerical features, e.g. frequencies and lengths and qrels at the level of document-query pair.

Only laboratory experiments based on experimental datasets were considered in this paper. Nevertheless, nothing in principle prevents from applying SEM to contexts other than laboratory, such as user studies or naturalistic studies reported in Section 2.

4.1 Data Preparation

To be specific, we utilized two public learning-to-rank datasets:

- The Learning To Rank (LETOR) package (version 4.0) consists of three corpora and nine query sets as reported by Qin et al. [2010]. In our experiments, the Gov2 corpus and the 2007 Million Query track’s query set were utilized. Table 2 summarizes the 46 features of LETOR.

- The Microsoft Learning-to-Rank (MSLR) package consists of two large-scale datasets. One dataset has 30,000 queries and 3,771,126 documents, the other dataset is a random sample. We utilized the random sample that has 10,000 and 1,200,193 documents. Table 3 summarizes the features of MSLR utilized in this paper. Liu [2011] reports further information.

The features of LETOR and MSLR were utilized to implement the manifest variables of the structural equation models tested in the experiments reported in this section.

5The complete list of features are available at http://research.microsoft.com/en-us/projects/mslr/feature.aspx.
Figure 1: Highly collinear variables in LETOR. Each connected subgraph represents a subset of highly collinear variables. An edge was added when the Pearson correlation coefficient was 0.90 or more.

However, before investigating some structural equation models, the data were analyzed as for collinearity and outliers.

If the analysis is performed at the level of query and not at the level of document, the linked records can be grouped by run and query, and the features are averaged for each group. Each resulting record was then linked to the performance scores of the run for the query.

We found high collinearity (0.90+) between some variables of both datasets. As a first simple solution, one variable can be kept for each cluster of collinear variables and the other variables can be ignored. We removed the most specific features and kept the most general; for example, we kept term frequency within a document and removed term frequency within the document title. The criteria to ignore a variable depends on the ease of interpretation of the SEM results, since the results will not significantly change with the ignored variables. Table 4 summarizes what was ignored and what was kept.

The outliers of a variable have been mapped to the mean value of the variable to reduce the overall variability. We also applied $\log(x + \min x + 1)$ to all exogenous variables $x$ to reduce non-normality and variability of the distribution of manifest exogenous variables and to make data closer to normal distribution. It is a standard practice in Statistics. There are other transformations. Usually, a transformation improves how well a particular SEM fits the data.
Table 2: Features for the Gov2 corpus; for each feature, an identifier, a short name, and a description are provided. Symbols: \( t \) is a term, \( Q \) is a query, \( D \) is a document. Notes: DIR = “Dirichlet smoothing”, JM = “Jelinek-Mercer smoothing”, ABS = “Absolute discount smoothing”.

| Id | Short name | Feature description |
|----|------------|---------------------|
| 1  | bodytfsum  | \( \sum_{t \in D} \text{TF}(t, D) \) in body |
| 2  | anchor tfsum | \( \sum_{t \in D} \text{TF}(t, D) \) in anchor |
| 3  | title tfsum  | \( \sum_{t \in D} \text{TF}(t, D) \) in titlebody |
| 4  | ur ltfsum  | \( \sum_{t \in D} \text{TF}(t, D) \) in URL |
| 5  | tfsum  | \( \sum_{t \in D} \text{TF}(t, D) \) in \( D \) |
| 6  | body idfsum | \( \sum_{t \in D} \text{IDF}(t) \) in body |
| 7  | anchor idfsum | \( \sum_{t \in D} \text{IDF}(t) \) in anchor |
| 8  | title idfsum  | \( \sum_{t \in D} \text{IDF}(t) \) in titlebody |
| 9  | url idfsum  | \( \sum_{t \in D} \text{IDF}(t) \) in URL |
| 10 | idfsum  | \( \sum_{t \in D} \text{IDF}(t) \) in \( D \) |
| 11 | body tfidfsum | \( \sum_{t \in D} \text{TF-IDF}(t, D) \) in body |
| 12 | anchor tfidfsum | \( \sum_{t \in D} \text{TF-IDF}(t, D) \) in anchor |
| 13 | title tfidfsum | \( \sum_{t \in D} \text{TF-IDF}(t, D) \) in titlebody |
| 14 | url tfidfsum | \( \sum_{t \in D} \text{TF-IDF}(t, D) \) in URL |
| 15 | tfidfsum | \( \sum_{t \in D} \text{TF-IDF}(t, D) \) in \( D \) |
| 16 | body doclen | \( \sum_{t \in D} \text{LENGTH}(D) \) in body |
| 17 | anchor doc len | \( \sum_{t \in D} \text{LENGTH}(D) \) in anchor |
| 18 | title doclen | \( \sum_{t \in D} \text{LENGTH}(D) \) in titlebody |
| 19 | url doclen | \( \sum_{t \in D} \text{LENGTH}(D) \) in URL |
| 20 | doc len | \( \sum_{t \in D} \text{LENGTH}(D) \) in \( D \) |
| 21 | body bm25 | \( \sum_{t \in D} \text{BM25}(t, D) \) in body |
| 22 | anchor bm25 | \( \sum_{t \in D} \text{BM25}(t, D) \) in anchor |
| 23 | title bm25 | \( \sum_{t \in D} \text{BM25}(t, D) \) in titlebody |
| 24 | url bm25 | \( \sum_{t \in D} \text{BM25}(t, D) \) in URL |
| 25 | bm25 | \( \sum_{t \in D} \text{BM25}(t, D) \) in \( D \) |
| 26 | body lm ir abs | \( \sum_{t \in D} \text{LMIRABS}(t, D) \) in body |
| 27 | anchor lm ir abs | \( \sum_{t \in D} \text{LMIRABS}(t, D) \) in anchor |
| 28 | title lm ir abs | \( \sum_{t \in D} \text{LMIRABS}(t, D) \) in titlebody |
| 29 | url lm ir abs | \( \sum_{t \in D} \text{LMIRABS}(t, D) \) in URL |
| 30 | lm ir abs | \( \sum_{t \in D} \text{LMIRABS}(t, D) \) in \( D \) |
| 31 | body lm ir dir | \( \sum_{t \in D} \text{LMIRDIR}(t, D) \) in body |
| 32 | anchor lm ir dir | \( \sum_{t \in D} \text{LMIRDIR}(t, D) \) in anchor |
| 33 | title lm ir dir | \( \sum_{t \in D} \text{LMIRDIR}(t, D) \) in titlebody |
| 34 | url lm ir dir | \( \sum_{t \in D} \text{LMIRDIR}(t, D) \) in URL |
| 35 | lm ir dir | \( \sum_{t \in D} \text{LMIRDIR}(t, D) \) in \( D \) |
| 36 | body lm ir jm | \( \sum_{t \in D} \text{LMIRJM}(t, D) \) in body |
| 37 | anchor lm ir jm | \( \sum_{t \in D} \text{LMIRJM}(t, D) \) in anchor |
| 38 | title lm ir jm | \( \sum_{t \in D} \text{LMIRJM}(t, D) \) in titlebody |
| 39 | url lm ir jm | \( \sum_{t \in D} \text{LMIRJM}(t, D) \) in URL |
| 40 | lm ir jm | \( \sum_{t \in D} \text{LMIRJM}(t, D) \) in \( D \) |
| 41 | pagerank | PageRank of \( D \) |
| 42 | in links | Number of in-links of \( D \) |
| 43 | out links | Number of out-links of \( D \) |
| 44 | url depth | Number of slashes of the \( D \)'s Uniform Resource Locator (URL) |
| 45 | url len | Length of the \( D \)'s URL |
| 46 | children | Number of children of \( D \) |
| Id | Short name | Description |
|----|------------|-------------|
| 1  | qtnbody    | covered query term number body |
| 2  | qtnanchor  | covered query term number anchor |
| 3  | qtnanchor  | covered query term number title |
| 4  | qtnurl     | covered query term number url |
| 5  | qtn        | covered query term number whole document |
| 12 | streamlenanchor | stream length anchor |
| 13 | streamlentitle | stream length title |
| 14 | streamlenurl  | stream length url |
| 15 | streamlen    | stream length whole document |
| 46 | tfnstreamlenbody | sum of stream length normalized term frequency body |
| 47 | tfnstreamlenanchor | sum of stream length normalized term frequency anchor |
| 48 | tfnstreamlentitle | sum of stream length normalized term frequency title |
| 50 | tfnstreamlen | sum of stream length normalized term frequency whole document |
| 71 | tfidfsumanchor | sum of Term Frequency (TF) × Inverse Document Frequency (IDF) (TFIDF) anchor |
| 73 | tfidfsumtitle | sum of TFIDF title |
| 74 | tfidfsumurl  | sum of TFIDF url |
| 75 | tfidfsum    | sum of TFIDF whole document |
| 106 | bm25body   | BM25 body |
| 107 | bm25anchor | BM25 anchor |
| 108 | bm25title  | BM25 title |
| 109 | bm25url    | BM25 url |
| 110 | bm25       | BM25 whole document |
| 111 | lmirabsbody | LMIR.ABS body (language model approach for IR with absolute discounting smoothing) |
| 113 | lmirabstitle | LMIR.ABS title |
| 114 | lmirabsurl | LMIR.ABS url |
| 115 | lmirabs    | LMIR.ABS whole document |
| 116 | lmirdiranchor | LMIR.DIR anchor (language model approach for IR with Bayesian smoothing using Dirichlet priors) |
| 118 | lmirdirtitle | LMIR.DIR title |
| 119 | lmirdirurl | LMIR.DIR url |
| 120 | lmirdir    | LMIR.DIR whole document |
| 126 | slashes    | Number of slashes in URL |
| 127 | urllen    | Length of URL |
| 124 | inlink    | Inlink number |
| 129 | outlink    | Outlink number |
| 130 | pagerank  | PageRank |
| 131 | siterrank  | SiteRank (Site level PageRank) |
| 132 | quality    | QualityScore (the quality score of a web page; the score is outputted by a web page quality classifier) |
| 133 | badness    | QualityScore2 (the quality score of a web page; the score is outputted by a web page quality classifier, which measures the badness of a web page) |
| 134 | query_urlclickcount | query-url click count (the click count of a query-url pair at a search engine in a period) |
| 135 | urlclickcount | url click count (the click count of an url aggregated from user browsing data in a period) |
| 136 | url_dwell_time | url dwell time (the average dwell time of an url aggregated from user browsing data in a period) |

Table 3: Exogenous manifest variables of the MSLR dataset (query 22636) kept for the analysis. The complete list is available at http://research.microsoft.com/en-us/projects/mslr/feature.aspx.
Table 4: Highly collinear variables kept for or ignored from analysis.

| Variable kept          | Variables ignored                              |
|------------------------|-----------------------------------------------|
| anchorltfidfsum        | anchorltfidfsum                               |
| titlelmirdir           | urltfidfsum, urltfsum                         |
| titleltfidfsum         | titleltfidfsum                                |
| tfidfsum               | bodytfidfsum                                  |
| tfsum                  | bodytfsum                                     |
| bodybm25               | anchorlmirjm                                  |
| lmirdir                | bodylmirjm, urllmirdir                        |
| lmirjm                 | titlelmirjm, urlbm25, anchorbm25              |
| bodylmirabs            | titlelmirabs                                  |
| lmirabs                | anchorlmirjd, bodylmirjd                      |
| titlebm25              | urllmirjm                                     |
| doclen                 | bodydoclen                                   |

Kurtosis (i.e. heavier/lighter tails and a higher/lower peak than normal) and skewness (i.e. asymmetry about normal mean) were reduced, yet not completely eliminated. However, “children” of LETOR was still very skewed and leptokurtic. QQ-plotting allowed us to see that the lack of normality was due to a very few large values while the others were null; this variable was then ignored. The other variables exhibit lack of normality at very high or very low values. The middle values have a good fit with normality.

The manifest variables of LETOR have well-scaled variances, since the scale is 8:1, which is acceptable. Were the scale greater than hundreds, the values of the variables exhibiting the smallest variance should be multiplied by a certain factor until the scale becomes small.

Another approach can be based on reimplementing publicly documented retrieval algorithms. The difference between these two approaches lies in the degree of control of the retrieval functions. When using public datasets and runs, the researcher investigates the retrieval functions designed and implemented by other researchers, thus counting on the available documentation. When reimplementing publicly documented retrieval algorithms, the researcher may make decisions about some steps of indexing and retrieval which may make the implemented retrieval functions slightly different from similar functions. In particular, the latter approach allows the researcher to investigate his own retrieval functions. The experiments that are reported in Section 4.2 implemented the approach based on the reuse and combination of public datasets. In particular, two publicly available runs submitted to the Text REtrieval Conference (TREC) website and a public learning-to-rank dataset were utilized. We reproduced the runs obtained by a retrieval system based on BM25 and those obtained by a retrieval system based on TFIDF using the TIPSTER test collection. In our experiments, the discs 4 and 5 of the TIPSTER collection and the query sets of TREC-6, TREC-7 and TREC-8 were utilized to perform the experiments.
4.2 Use of Runs and Learning To Rank Datasets

Some structural equation models that are investigated in this paper include endogenous variables based on precision. Because precision is needed, document ranking was necessary. To obtain document ranking, we utilized two runs submitted to the TREC website for the 2007 Million Query track described by Allan et al. [2007]. Two runs described by Hiemstra et al. [2007] and produced using a full-text index built by Lucene [McCandless et al., 2010] were reused in our experiments to generate the endogenous variables of some structural equation models of this paper. One run was based on the Vector Space Model (VSM) (UAMsT07MTeVS) and the other was based on the Language Model (LM) (UAMsT07MTeLM).

Learning To Rank datasets were joined to the runs; in particular, for each run, every query-document pair of a run was linked to the corresponding record of document and query features. Thus, we had one record of features for each run, query, and document that can be in turn linked to the endogenous manifest variables that can measure retrieval effectiveness; we utilized the ratio between the numeric value of qrel and document rank. Each record of a run was joined with the corresponding record of features; for example, each record of UAMsT07MTeVS that refers to query $t$ and document $d$ was joined with the record of LETOR that refers to $t$ and $d$. In this way, each record of a run was an extended description of a retrieved document. As for LETOR, we considered query 5440, for both runs, because the number of retrieved documents was relatively high (about 80 documents), thus allowing us to perform the experiments with a non-small sample.

The MSLR dataset was investigated through query 22636, which is related to a relatively high number of cases (809) and all the five relevance degrees were assigned to the cases. Two variables were highly collinear if the correlation was 0.975 or more [Kline, 2015]. Some methods are suggested in the literature, yet thresholds are empirically chosen. Something similar happens with p-values which are compared with standard threshold (e.g. 0.01 or 0.05). In the paper, the thresholds were chosen by visual inspection; the threshold was the minimum value that induces disconnected and complete subgraphs of manifest variables as depicted by Figs. 1 and 2. The clusters of highly collinear variables are depicted in Fig. 2. After ignoring the highly collinear variables, the variables involved during the analysis are reported in Table 3. To reduce lack of normality of the remaining variables, the transformation $\log(x + \min(x) + 1)$ was applied to all exogenous variables. Unlike LETOR, the ratio between the maximum variance and the minimum variance was very high (12/0.001) in MSLR. As the large distance between maximum variance and minimum variance would cause problems during parameter estimation, it was progressively reduced by doubling the variable with minimum variance until the ratio was not greater than 10. (see the algorithm of Fig. 3).

In the following sections, some analysis of experimental retrieval results have been illustrated.
4.3 Testing What Affects Effectiveness

Consider the manifest variables of UAmsT07MTeVS and UAmsT07MTeLM after applying the logarithmic transformation to reduce non-normality.

As mentioned above, the endogenous variable was the ratio between the numeric value of qrel and document rank. In order to reduce the variability, a log-transformation was applied to this ratio too. As the numeric value of qrel may be zero and a log-transformation cannot be applied to zero, the actual transformation was \( Y = \log(qrel + 1)/(\text{rank} + 1) \) where qrel is the numeric value of qrel. The argument of the logarithmic function is positive when the document at the rank of the denominator is relevant and decreases when rank increases. It is a precision measure at the level of document since it is the contribution of a document to precision. Instead, \( P@r \) is a measure of precision at the level of document list since it is the precision while the sublist of
After preparing the data, we looked for the best path model fitting the exogenous variables to the endogenous variable that measure retrieval effectiveness. To this end, a process of experimenting with various path models was performed until a good fit was found. In the experiments of this paper, the path model for UAmst07MTeVS was

\[ Y \leftarrow \log(\text{bodybm25} + 1) + \log(\text{titlebm25} + 1) + \log(\text{anchortfsum} + 1) \]

and that for UAmst07MTeLM was

\[ Y \leftarrow \log(\text{bodybm25} + 1) + \log(\text{lmirjm} + 1) + \log(\text{tfsum} + 1) \]

Table 5: The first 16 principal components of the MSLR rescaled variables for query 22636

|        | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12 | 13 | 14 | 15 |
|--------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| qntbody| -1 | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 0  |
| qntanchor| 0  | -1 | -1 | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 0  | -1 |
| qntitle| -1 | 0  | 0  | 0  | 0  | 0  | 1  | 0  | -1 | 0  | 0  | -1 | 1  | 0  | 0  |
| qnturl| 0  | -1 | 1  | 0  | -1 | 0  | 0  | 0  | -1 | 0  | 0  | -1 | -1 | 1  | 0  | 0  |
| qtn| -1 | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 0  | -1 | -1 | 0  | 0  | 0  |
| strmrlenanchor| 0  | -1 | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | -1 | -1 | 0  | 0  | 0  |
| strmlen| -1 | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| strmendlenanchor| 0  | -1 | -1 | 1  | 0  | 0  | 0  | 0  | 0  | 0  | -1 | -1 | 0  | 0  | 0  |
| strmendlen| -1 | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| tfnstrmrlensumbody| -1 | 0  | 0  | 1  | 0  | 0  | 0  | 1  | 1  | 0  | 1  | 0  | 0  | 1  | 0  |
| tfnstrmrlensumanchor| 0  | -1 | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| tfnstrmrlensumtitle| -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| tfnstrmrlensum| -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| tdiffsumanchor| 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| tdiffsum| -1 | 0  | 0  | 0  | 0  | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| bm25body| -1 | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 1  |
| bm25anchor| 0  | -1 | -1 | 1  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  |
| bm25title| -1 | 0  | 0  | 0  | 0  | 0  | 0  | -1 | 1  | 0  | 0  | -1 | 0  | 0  | 0  |
| bm25url| 0  | -1 | 1  | 0  | -1 | 0  | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  |
| lmirsbody| -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| lmirsurl| 0  | -1 | 1  | 0  | -1 | 0  | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  |
| lmirs| -1 | 0  | 0  | 0  | 0  | 0  | 0  | -1 | 0  | 0  | -1 | 0  | 0  | 0  | 0  |
| lmirsl| -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| lmirl| -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  | 0  |
| lmirlurl| 0  | -1 | 1  | -1 | 0  | 0  | 0  | 1  | -1 | 0  | 1  | 1  | 1  | 1  | 1  |
| lmirl| -1 | 0  | 0  | 0  | 0  | 0  | -1 | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 0  |
| slakes| -1 | 0  | 0  | 0  | 0  | 0  | 1  | 0  | 0  | 1  | 0  | 0  | 0  | 0  | 0  |
| urlen| 0  | -1 | 1  | 1  | 0  | 0  | 0  | 0  | 1  | 0  | -1 | 0  | 0  | 0  | 0  |
| urllen| 0  | -1 | 1  | 0  | 0  | 0  | 0  | 1  | 1  | 1  | -1 | 0  | -1 | 1  | 0  |
| inlink| 0  | -1 | -1 | 0  | 1  | 1  | 0  | -1 | -1 | 0  | -1 | -1 | 0  | -1 | -1 |
| outlink| 0  | -1 | 0  | -1 | 0  | -1 | 0  | 1  | 1  | 1  | 1  | 0  | -1 | 0  | -1 |
| pagerank| 0  | 0  | -1 | -1 | -1 | 1  | -1 | -1 | -1 | -1 | 0  | 0  | -1 | 1  | 0  |
| sitranl| 0  | -1 | -1 | 1  | 0  | 0  | 0  | 1  | 1  | 1  | -1 | -1 | -1 | -1 | 0  |
| quality| 1  | 0  | 0  | 1  | 0  | 0  | 1  | 0  | 1  | 1  | 1  | 0  | -1 | 1  | 0  |
| badness| 0  | 0  | 1  | 1  | 0  | -1 | -1 | -1 | 0  | 1  | 0  | -1 | -1 | 0  | -1 |
| query_url_clickcount| 0  | 0  | 0  | 0  | -1 | 0  | -1 | -1 | -1 | -1 | 0  | 0  | 1  | 1  | 0  |
| url_clickcount| 0  | 1  | -1 | -1 | -1 | 0  | 0  | 1  | 1  | 1  | -1 | -1 | -1 | -1 | 0  |
| url_dwell_time| 0  | 1  | -1 | 0  | -1 | 0  | 0  | 1  | 0  | 0  | -1 | -1 | -1 | -1 | 0  |

the top \( r \) documents is scanned. The \( Y \) defined above is preferable to \( P@r \) because the analysis performed on UAmsT07MTeVS and UAmsT07MTeLM was at the level of document – the LETOR records were indeed joined to documents and not to lists. 
Require: Dataset of $k$ manifest variables, $X_1, \ldots, X_k$

ingscaled ← TRUE

while illscaled do
    $i_{\text{max}} \leftarrow \arg_{i=1,\ldots,k} \max \text{var}(X_i)$
    $i_{\text{min}} \leftarrow \arg_{i=1,\ldots,k} \min \text{var}(X_i)$
    if $\text{var}(X_{i_{\text{max}}}) / \text{var}(X_{i_{\text{min}}}) \leq 10$ then
        illscaled ← FALSE
    else
        $X_{i_{\text{min}}} \leftarrow 2X_{i_{\text{min}}}$
    end if
end while

Figure 3: The algorithm used to rescale the variables until the variances were no longer ill-scaled.

Two structural equation models have been tested in the experiments:

$$Y = B_{\text{bodybm25}} \log(\text{bodybm25} + 1) +$$
$$B_{\text{titlebm25}} \log(\text{titlebm25} + 1) +$$
$$B_{\text{anchortfsum}} \log(\text{anchortfsum} + 1)$$

for UAmsT07MTeVS and

$$Y = B_{\text{bodybm25}} \log(\text{bodybm25} + 1) +$$
$$B_{\text{lmirjm}} \log(\text{lmirjm} + 1) +$$
$$B_{\text{tfsum}} \log(\text{tfsum} + 1)$$

for UAmsT07MTeLM. An exogenous variable was significant when its regression coefficient was statistically significant ($p$-value $\approx 0$); the variables of the two structural equation models have significant regression coefficients, in particular,

$$B_{\text{bodybm25}} = 6.55$$
$$B_{\text{titlebm25}} = 5.10$$
$$B_{\text{anchortfsum}} = -1.67$$

for UAmsT07MTeVS and

$$B_{\text{tfsum}} = 1.89$$
$$B_{\text{lmirjm}} = 9.10$$
$$B_{\text{bodybm25}} = 1.45$$
for UAmsT07MTeLM. The beta coefficients are

\[ \beta_{\text{bodybm25}} = 0.44 \]
\[ \beta_{\text{titlebm25}} = 0.64 \]
\[ \beta_{\text{anchortfsum}} = -0.10 \]

for UAmsT07MTeVS and

\[ \beta_{\text{dfsum}} = 0.15 \]
\[ \beta_{\text{lmirjm}} = 0.87 \]
\[ \beta_{\text{bodybm25}} = 0.10 \]

for UAmsT07MTeLM, thus confirming the role played by BM25 – early introduced by Robertson and Walker [1994] – and LM – proposed by Ponte and Croft [1998] – for these two runs. Using the proportion of variance explained by all manifest variables with direct effects on the endogenous variable, we have a measure of goodness-of-fit \( R^2 \). The \( R^2 \)'s values of the two models were 0.85 and 0.90 respectively for UAmsT07MTeLM and UAmsT07MTeVS, thus suggesting a good fit of the endogenous variable.

Finding the best path models was not a straightforward process. Indeed, given the endogenous variable, a path model is defined on the basis of a subset of exogenous variables, therefore, the best path model was the subset of exogenous variables that best fit the endogenous variable. Moreover, the process to find the best fit is manual and based on the researcher’s knowledge of the application domain. The difficulty of finding the best fit is hampered by the potential complete enumeration all the possible subsets, whose exponential number is \( 2^N \) to the power of the number of exogenous variables, the latter requiring an infeasible amount of work even for not large numbers. To cope with this exponential order, the semantics of the exogenous variables and the description of the retrieval algorithm utilized to produce a run helped select the most appropriate variables; for example, pagerank, which was computed by the PageRank algorithm introduced by Brin and Page [1998], is unlikely to correlate with effectiveness when UAmsT07MTeVS is considered, whereas tfsum would be more appropriate.

Although the researcher’s knowledge of the application domain seems necessary to limit the space of subsets of exogenous variables, it is still likely that some subsets might be missed, thus making the selected structural equation models less than optimal.

As for UAmsT07MTeLM, the type of smoothing plays a crucial role because the effectiveness of the exogenous variable explaining the endogenous variable changes with smoothing technique. Indeed, \( R^2 \) significantly decreases if lmirjm is replaced with lmirdir or lmirabs, the latter being an outcome explained by the negative correlation between lmirjm and lmirdir (p-value < 0.05) and that between lmirjm and lmirabs.
In contrast, the importance of bodybm25, which is the backbone of the probabilistic models, for the VSM-based run is worth noting especially if it is compared with the importance of the variables significantly related to the VSM such as anchortfsum. However, the important role played by bm25 should not come as a complete surprise. The sum of TFIDF weights (tfdifsum) provided by LETOR has been computed using a mathematical formulation different from the formulation implemented by modern VSM retrieval systems such as Lucene, which was used in the experiments reported by Hiemstra et al. [2007]. Indeed, the Lucene formulation is more similar to BM25 than to the LETOR’s tfidfsum, thus explaining why bodybm25 explains retrieval effectiveness in the VSM-based run. The small statistical correlation between bodytfdifsum and bodybm25 has further confirmed that their mathematical formulations were different. The main reason for this discrepancy was due to doclen, which is the most correlated variable with both bodytfdifsum and bodybm25 (both p-values were not greater than 0.01): the correlation between doclen and bodytfdifsum was positive, whereas that between doclen and bodybm25 was negative.

The role played by BM25 in the VSM-based run mentioned above might be considered an example of what SEM can suggest when applied to investigate experimental results. Some variables that are absent from a ranking function may have a role in a revised ranking function because they are significantly related to retrieval effectiveness in so far as its beta coefficient suggests. The revised ranking function may include the new variable using some mathematical or algorithmic rule decided by the researcher hoping that the new variable can boost the ranks of retrieved relevant documents or the retrieval of additional relevant documents.

The goodness-of-fit changes when the LM scores utilized as exogenous variables are those calculated from document parts other than the complete document; for example, if lmirm is replaced with bodylmirm, $R^2$ decreases. Similarly, the effectiveness of BM25 in explaining the endogenous variable of UAmsT07MTeVS depends on the document part from which the estimation data are extracted; for example, when bodybm25 is replaced with bm25 the goodness-of-fit decreases considerably, thus suggesting that the distribution of the terms significantly changes when it is estimated from different document parts.

Structural equation modeling depends on query and on run; indeed, testing the models found for query 5440 and applied to UAmsT07MTeLM and UAmsT07MTeVS for another query (e.g. 2297) gave unsatisfactory results as shown by the significant decrement of $R^2$. This outcome and the dependencies of the document parts from which estimation is performed are both an issue and a strength of the SEM-based approach to diagnose IR evaluation. On the one hand, it is an issue because a structural equation model has to be found for each retrieval algorithm (i.e. run) and for each query, and finding such a model requires an intellectual effort of the researcher who has to apply his expertise in the application domain being investigated by means of
SEM for each run and query. On the other hand, the adaptation of the structural equation model to both run and query can provide an in-depth description of the retrieval system’s performance for each query and can make the failure analysis at the level of query possible and effective. Such a dependency calls from fully or semi-automatic methods for generating and testing structural equation models that can support the IR researcher in analyzing the successes and the failures of a retrieval system.

4.4 Testing Latent Variables Behind Manifest Variables

In IR, researchers often assume the presence of latent variables such as relevance, authoritativeness (introduced by Brin and Page [1998] and Kleinberg [1999]) and elite-ness (introduced by Harter [1975]) behind the observed variables such as term frequencies and qrels. For example, the fact that relevance cannot be reduced to aboutness\(^6\) and that further dimensions of relevance such as document authoritativeness and quality should be considered in a retrieval function is by now well accepted. Another example is the metaphor of the LM approach introduced by Ponte and Croft [1998]. It assumes that both the authors of a document and the users who assess the document as relevant write the document and queries, respectively, that are about the same query, thus establishing a relationship between relevance and aboutness.

Another example of the use of CFA in IR is the investigation of the coexistence of authoritativeness and aboutness as two distinct latent variables in the same document. A document can be viewed as authoritative when is able to be trusted as being accurate, true or reliable; other terms that are used to describe this document features are credibility or veracity; in contextual IR, authoritativeness can be viewed as a factor of document quality [Melucci, 2012] and can be measured by, for example, PageRank. The following model in which qrel can be a manifestation of both latent variables may model the coexistence of authoritativeness and aboutness as two distinct latent variables in the same document:

\[
\begin{align*}
\text{authoritativeness} & \rightarrow \text{pagerank} + \text{indegree} + \text{urldensity} + \text{qrel} \tag{2} \\
\text{aboutness} & \rightarrow \text{doclen} + \text{bm25} + \text{qrel} \tag{3} \\
\text{authoritativeness} & \leftrightarrow \text{aboutness} \tag{4}
\end{align*}
\]

where the regression coefficients of (2) are

\[
\begin{align*}
P_{\text{pagerank}} &= 0.044 \\
P_{\text{indegree}} &= 0.006 \\
P_{\text{urldensity}} &= -0.043 \\
P_{\text{qrel}} &= 0.022
\end{align*}
\]

\(^6\)The property of a document which concerns a certain topic.
and the regression coefficients of (3) are

\[ B_{\text{doclen}} = 0.137 \]
\[ B_{\text{bm25}} = -0.047 \]
\[ B_{\text{qrel}} = 0.396 \]

These coefficients are statistically significant with p-value < 0.01 except for \( B_{\text{qrel}} \) of (2). The correlation between authoritativeness and aboutness is insignificant. This model passes the chi-square exact-fit test (p-value = 0.116) as confirmed by CFI = 0.934. It also passes the approximate fit test since RMSEA = 0.089 (p-value = 0.212).

Latent variables were investigated also using MSLR. Besides including many more variables than LETOR, MSLR also includes variables about the behaviour of the users who visited the pages described in the dataset and a couple of variables about the quality of the pages visited by the users. The variety of manifest variables of MSLR allowed us to make some hypotheses about the latent variables that may affect retrieval effectiveness. In particular, it was hypothesized that four latent variables, i.e. content, link, graph, page and user, may explain the manifest endogenous variable named “qrel” that encodes retrieval effectiveness (qrel ranges from 0 to 4). The latent variable “content” was about the informative content (i.e. keywords) of the pages that matched the query’s informative content. The latent variable “link” was about the informative content stored in the URLs and in the link anchors that matched the query’s informative content. The latent variable “graph” was about the graphical properties of the World Wide Web (WWW) node that corresponds to the page. The latent variable “user” was about the behaviour of the user who visited the page. The latent variable “page” was about the quality of the page. Thus, we have the following structural equation model:

\[
\begin{align*}
\text{qrel} & \leftarrow \text{content} + \text{link} + \text{graph} + \text{quality} + \text{user} \\
\text{content} & \rightarrow \text{qtnbody} + \text{qntitle} + \text{qtn} + \text{strmlentitle} + \\
& \quad \text{strmlen} + \text{tfnstrmlensumbody} + \text{tfnstrmlensumtitle} + \\
& \quad \text{+tfnstrmlensum} + \text{tfdsumtitle} + \text{tfdsum} + \\
& \quad \text{bm25title} + \text{bm25} + \text{lmirabsbody} + \\
& \quad \text{lmirabstitle} + \text{lmirabs} + \text{lmirdirtitle} \\
\text{graph} & \rightarrow \text{pagerank} + \text{inlink} + \text{outlink} + \text{siterank} \\
\text{link} & \rightarrow \text{qtnurl} + \text{strmlenanchor} + \text{strmlenurl} + \\
& \quad \text{+tfnstrmlensumanchor} + \text{tfdsumanchor} + \text{tfdsumurl} + \\
& \quad \text{+bm25anchor} + \text{bm25url} + \text{lmirabsurl} + \\
& \quad \text{lmirdiranchor} + \text{lmirdirurl} \\
\text{page} & \rightarrow \text{quality} + \text{badness} \\
\text{user} & \rightarrow \text{query}_\text{url}_\text{clickcount} + \text{url}_\text{clickcount}
\end{align*}
\]
The goodness-of-fit analysis of the structural equation model above came to contradictory indexes. CFI and TLI were relatively high (0.921 and 0.913, respectively) yet RMSEA was not very small (0.114) and its p-value was approximately zero, thus suggesting that the close fit hypothesis should be rejected. Besides, only the latent variable “user” was a significant latent variable explaining relevance (i.e. qrel). The regression coefficient was indeed 0.230 (p-value was approximately zero), thus suggesting that the number of clicks was a good predictor of relevance and that content, graph, link and page were little significant in explaining relevance. As for the relationships between latent variables and manifest variables, the variables based on “qtn”, TFIDF and LM were the most significant in explaining content, inlink was the most significant in explaining graph, the variables based on “anchor” in explaining url, quality in explaining page, and url|clickcount was the most significant manifest variable in explaining user.

Another issue of SEM is that a latent variable might not correspond to an entity conceived by everyone in only one way; for example, eliteness might be conceived as a small subset of terms by a researcher, whereas it might be conceived as a more complex entity by another researcher. Since latent variable names are usually nouns, they suffer from the usual natural language drawbacks; for example, a latent variable name may be a synonym of another name or may be polysemous and carry more than one meaning at the same time.

Authoritativeness and aboutness are unrelated as shown by (4). This outcome confirms the early literature on the use of link analysis in IR in that authoritativeness and aboutness should be considered as distinct dimensions of relevance, capturing different user’s information needs; some users may require authoritative documents which might be little relevant while other users may require relevant documents yet little authoritative. The lack of relationship between authoritativeness and aboutness can also be observed by the lack of significance of the regression coefficient of qrel in (3) as opposed to the significance of qrel in (2), thus suggesting that qrel can be a signal of aboutness and not of authoritativeness.

Indegree and pagerank are both significant manifestations of authoritativeness. One reason for this simultaneous, significant manifestation may be due to the relationship between pagerank and indegree. Although it is a more complex algorithm than simply counting in-links, PageRank and indegree are strongly correlated (Pearson’s product-moment correlation comes out to be 0.832 with p-value ≈ 0). To check the hypothesis that pagerank might be removed from (2), the fit of the structural equation model introduced above has been recalculated without pagerank, thus obtaining very similar results: exact fit test passed with p-value = 0.570; approximate fit test passed with p-value = 0.662; CFI = 1.

The structural equation model that relates relevance degree (i.e. qrel) to five latent variables (i.e. content, user, link, graph, and quality) was only partially satisfactory, at least as far as query 22636 of MSLR is concerned. The unsatisfactory fit of this structural equation model suggests that the latent variables causing qrel might be less
straightforward than those encoded by content, user, link, graph, and page, the latter often being utilized to model contextual search according to Melucci [2012], O’Brien and Toms [2013] and Park [2014]. For example, a manifest variable should be related to more than one latent variable in an improved structural equation model; however, the addition of relationships between variables might make a model unidentifiable.

To overcome the limitations on the generality of the results caused by the utilisation of one query, automated tools that perform such an analysis for many queries and datasets should be designed and implemented. As regards the goodness-of-fit of the structural equation model, although the approximate close indexes (CFI and TLI) were relatively high, other statistics suggested that better models should be found (for example RMSEA was not very small). Unfortunately, SEM cannot straightforwardly suggest the correct and best model unless the researcher helps to find such a model by using his knowledge of the application domain, yet some help can be given by the analysis of residuals in the covariance matrix.

4.5 Effect of Query Terms

In this section, the impact of the query term weights of Lucene’s implementation of the VSM-based retrieval function and that of the BM25-based retrieval function will be investigated. The VSM-based retrieval function is a modification of the classical VSM retrieval function and was applied for each query $Q$ and document $D$ as follows:

$$\sum_{t \in Q} dtw_{t,D} qtw_{t,Q} coord_{Q,D} boost_t$$

where

- $dtw_{t,D} = tfidf_{t,D}$
- $qtw_{t,Q} = tfidf_{t,Q}$
- $coord_{Q,D} = \frac{|D \cap Q|}{|Q|}$
- $boost_t = 1$

On the other hand, the BM25-based run was obtained by the following retrieval function

$$\sum_{t \in Q} idf_t sat_{t,D}$$

33
where

\[
\text{idf}_{t,D} = \log \frac{N - \text{df}_t + 0.5}{\text{df}_t + 0.5}
\]

\[
\text{sat}_t = \frac{\text{tf}_{t,D}}{\text{K} + \text{tf}_{t,D}}
\]

\[
\text{K} = k_1 \left( 1 - b + \frac{\text{doclen}}{\text{avdoclen}} \right)
\]

For each query, two lists of documents were created – one list for each retrieval function. Each retrieved document has been associated to the assessment of relevance to the query and was joined to the components of the weight function of each query term. In particular, each document retrieved by the VSM-based retrieval function was joined to \( \text{dtw}_{t,D}, \text{qtw}_{t,Q}, \text{coord}_{Q,D}, \text{boost} \), for each query term \( t \), and each document retrieved by the BM25-based retrieval function was joined to \( \text{idf}_{t,sat_{t,D}} \) for each query term \( t \). Moreover, \( P@r \) was computed for each document retrieved at rank \( r \).

The following structural equation model was estimated as for the BM25-based run and query 305 (“Most Dangerous Vehicles: Which are the most crashworthy, and least crashworthy, passenger vehicles?”):

\[
\text{prec} \leftarrow \text{bm25}_{\text{crashworthy}} + \text{bm25}_{\text{dangerous}} + \text{bm25}_{\text{passenger}} + \text{bm25}_{\text{vehicles}}
\]

The regression coefficients are as follows\(^7\):

\[
B_{\text{bm25,dangerous}} = 0.016
\]
\[
B_{\text{bm25,passenger}} = 0.023
\]
\[
B_{\text{bm25,vehicles}} = 0.017
\]

As the p-values were approximately zero, the regression coefficients were significant; however, the fit was rather bad because of the low number of exogenous variables. Although the regression coefficients can be an interesting measure of the variation of \( \text{prec} \), the beta coefficients were of greater interest because they provide a measure of the importance of each variable controlling the other variables. In particular, the beta coefficients were:

\[
\beta_{\text{bm25,dangerous}} = 0.229
\]
\[
\beta_{\text{bm25,passenger}} = 0.397
\]
\[
\beta_{\text{bm25,vehicles}} = 0.342
\]

\(^7\)The coefficients of “crashworthy” are not reported because only one retrieved document was indexed by “crashworthy.”
To investigate this model further, the following structural equation model that replaces the BM25 weights with their components (i.e. idf and sat) was estimated:

\[ \text{prec} \leftarrow \text{idf}_{\text{dangerous}} + \text{sat}_{\text{dangerous}} + \text{idf}_{\text{passenger}} + \text{sat}_{\text{passenger}} + \text{idf}_{\text{vehicles}} + \text{sat}_{\text{vehicles}} \]

The regression coefficients are as follows:

\[
\begin{align*}
B_{\text{idf, dangerous}} &= 0.002 \\
B_{\text{idf, passenger}} &= 0.023 \\
B_{\text{idf, vehicles}} &= 0.018 \\
B_{\text{sat, dangerous}} &= 0.047 \\
B_{\text{sat, passenger}} &= 0.102 \\
B_{\text{sat, vehicles}} &= 0.082 
\end{align*}
\]

Except for \(B_{\text{idf, dangerous}}\), these coefficients are significant. The corresponding beta coefficients are as follows:

\[
\begin{align*}
\beta_{\text{idf, dangerous}} &= -0.035 \\
\beta_{\text{idf, passenger}} &= -0.323 \\
\beta_{\text{idf, vehicles}} &= -0.340 \\
\beta_{\text{sat, dangerous}} &= 0.301 \\
\beta_{\text{sat, passenger}} &= 0.813 \\
\beta_{\text{sat, vehicles}} &= 0.857 
\end{align*}
\]

The following structural equation model was estimated as for the VSM-based run:

\[ \text{prec} \leftarrow \text{dtw}_{\text{crashworthy}} + \text{dtw}_{\text{dangerous}} + \text{dtw}_{\text{passenger}} + \text{dtw}_{\text{vehicles}} + \text{qtw}_{\text{crashworthy}} + \text{qtw}_{\text{dangerous}} + \text{qtw}_{\text{passenger}} + \text{qtw}_{\text{vehicles}} \]

The regression coefficients are as follows and all were significant:

\[
\begin{align*}
B_{\text{dtw, dangerous}} &= 0.064 \\
B_{\text{dtw, passenger}} &= 0.095 \\
B_{\text{dtw, vehicles}} &= 0.078 
\end{align*}
\]
The beta coefficients were as follows:

\[
\begin{align*}
B_{qtw,dangerous} &= 0.088 \\
B_{qtw,passenger} &= 0.042 \\
B_{qtw,vehicles} &= 0.074
\end{align*}
\]

The beta coefficients were as follows:

\[
\begin{align*}
\beta_{dtw,dangerous} &= 0.341 \\
\beta_{dtw,passenger} &= 0.929 \\
\beta_{dtw,vehicles} &= 0.635
\end{align*}
\]

\[
\begin{align*}
\beta_{qtw,dangerous} &= 0.412 \\
\beta_{qtw,passenger} &= 0.205 \\
\beta_{qtw,vehicles} &= 0.331
\end{align*}
\]

The badness of fit of the structural equation models above depends on the low number of exogenous variables; the fit was very good when all the weight components were added to the model for each query term. A good fit may be useful for prediction purposes; however, it may be misleading when the role played by the BM25-based query term weights is of interest. It might be misleading because, if all the weight components were added to the model for each query term, the beta coefficients of the saturation weights would have the opposite sign of the BM25-based query term weights. The difference in sign between the beta coefficients of saturation and those of BM25 is counter-intuitive since both saturation and BM25 should be positively correlated to prec. However, the difference in sign is caused by the strong correlations between the weight components that make the beta coefficients negative. The high collinearity could be acceptable when the variables are due to natural processes such as the collinearity between height and weight. In the event, they are not caused by natural processes; on the contrary, they are caused by the mathematical formulation of the function which make BM25 functionally dependent on saturation and IDF. It follows that the exogenous variables of the weight components (e.g. IDF) should be ignored and not added to the structural equation model together with BM25 in the analysis.

The negative correlation between BM25 weights can be quite surprising since it is expected that all the query terms participate in increasing P@r. Instead, the results of the analysis suggest that when one query term contributes to retrieval effectiveness, another query term is detrimental – for query 305 and the BM25-based retrieval function at least. The beta coefficients of the four query terms above indicate the most important query terms as regards P@r when document ranking is performed by the BM25-based retrieval function. When the retrieval functions are compared, the regression coefficients have to be used.
5 Conclusions and Future Directions

The crucial point of the use of SEM in data analytics is the definition of the structural equation models that describe the observed data at their best. It would be desirable to always find the best structural equation model, that is the model that fit the data very well on the basis of statistically significant parameters and of a reasonable narrative – from the researcher’s perspective at least. However, the best model cannot always be found, since two or more models may fit the observed data well or no fitting model may be found at all. Another weakness is the need to define structural equation models (e.g. path models) starting from many manifest variables. Although the researcher’s judgment should always be considered, manually finding the best model requires a considerable intellectual effort and some automatic method – semi-automatic at least – would be desirable.

In the area of learning-to-rank, in particular, and in that of Machine Learning, in general, a number of procedures for selecting features and fitting functions have been developed [Liu, 2011]. Although these procedures should be considered with reference to the problem of defining and estimating structural equation models, the selection of the variables of a structural equation model is a more complex task than the definition of real functions of the scores and weights which are observed for documents and terms to the aims of learning to rank. Variable selection has to do with the description of the retrieval models such as the VSM, the language models and the probabilistic models; the question is how to represent a retrieval model in terms of variables, relationships and therefore in terms of a structural equation model.

Moreover, further research would be advisable to find methods that “translate” a structural equation model into rules of modification for a more effective retrieval model once the structural equation model has been found for the retrieval model. Indeed, the ultimate goal of the use of SEM in IR evaluation would be the transformation of a retrieval model into a new, more effective model. Such a transformation resembles what the approaches to learning-to-rank aim for, that is, a set of parameters of a real function mapping an independent multi-variate variable to a dependent univariate variable.

The potential of SEM is the capacity to combine latent variables with manifest variables. The ability of using latent variables that may be developed may lead to implementing some general hypotheses about IR (e.g. the role played by authoritativeness or search task) and their influence on retrieval effectiveness. This ability may have some desirable effects. On the one hand, it may facilitate the investigation of the processes of information seeking based on the quantitative analysis provided by SEM. On the other hand, it may help the researchers to explain the results gathered throughout the course of their experiments by using more effective statistical instruments than descriptive or inferential statistics.

One distinguishing feature of SEM is the graphical nature of a structural equation model; such a model can be communicated in spoken or written words because variables and causal relationships thereof may be viewed as concepts (e.g. nouns) and
associations (e.g. verbs). As a result of the graphical nature of a structural equation model, SEM may become a new language helping the researchers in IR to find more powerful descriptions and explanations of theoretical models and experimental results than traditional statistics.

Despite the potential expressed since the pioneering work by Wright [1918], some misunderstandings are still limiting the potential of SEM [Bollen and Pearl, 2013]. First, it is often believed that correlation implies causation and that a significant regression coefficient may be considered a strong signal that a variable is the cause of another variable. Instead, SEM cannot discover causal relationships other than the relationships already encoded in the researcher’s structural equation model. Second, SEM is often viewed as nothing but a complicated regression and ANOVA technique. Causal networks rather, allow the researchers to utilise a language that is not part of standard statistics for expressing their application domains differently from the way provided by regression and ANOVA [Pearl, 2009, 2012].
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