Magnetic Characterization of the Infinitene Molecule
Guglielmo Monaco, Riccardo Zanasi, and Francesco F. Summa*

ABSTRACT: The origin-independent current density induced by a perpendicular magnetic field in the infinitene molecule has been calculated, confirming the recently presented result by Orozco-Ic et al. (Phys. Chem. Chem. Phys. 2022, 24, 6404−6409) of two disjointed global current pathways along the edges formed by 24 carbon atoms having the form of the infinity symbol. The current strength has been assessed along the C−C bonds forming the two separate circuits, whose particular shape provides a diamagnetic exaltation which is only 73% of the expected value for this aromatic molecule. Through space currents have been found along the bond paths determined by the electron density gradient, whose strength is 10% that of the aromatic benzene ring current. It is shown that the pair of high-field 1H NMR experimental signals carry the signature of the two global currents, which are counterrotating inside the fjord regions with respect to the rim of the coronene subunits.

INTRODUCTION
The large family of polycyclic aromatic hydrocarbons (PAHs) has recently acquired a new member referred to as “infinitene” due to its helically twisted structure resembling that of the infinity symbol (∞).1 Even at first glance, infinitene looks to be a truly fascinating molecule, in particular with regard to some issues concerning the nature of its aromaticity in terms of the magnetic criterion.2 In fact, besides enhanced stability, specific reactivity, and bond equalization, it is well recognized that the magnetically induced current density is intimately linked with the aromatic concept and it is an essential ingredient for the interpretation of the magnetic response of conjugated π-systems, such as the nuclear magnetic shielding in NMR spectroscopy and the exaltation of diamagnetism.3,4 However, despite recent progress,5,6 the inference of the actual shape of the ring current in PAHs, starting from 1H NMR data or the calculations of a few nucleus-independent chemical shifts (NICSs),7 is not straightforward, and this is especially true for curved PAHs, such as infinitene.

Infinitene can be seen as two cleaved coronene ([6]-circulene) subunits, twisted as two homochiral helices and stitched together by both their ends, in such a way that the rim of one coronene is attached to the hub of the other, forming two circuits of equal length containing 24 carbon atoms each. For coronene it is known that two counterrotating ring currents are induced by a perpendicular magnetic field, one strongly diatropic on the rim and the other weakly paratropic on the hub, which provide evidence for a resultant global aromaticity of the molecule.8 Therefore, a number of questions concerning the shape and strength of ring currents (if any) arise:
(i) What pathways do the currents travel through?
(ii) Are they global, or local to Clar sextets?
(iii) Which tropicity do they display?
(iv) How do their strengths compare with the benzene ring current?
(v) How large is the exaltation of diamagnetism for this aromatic molecule?
(vi) How can the high-field 1H NMR signals be justified on the basis of the actual current tropicity?

Nowadays, there exist powerful methods that can be readily used to solve the problem by calculating directly the magnetically induced current density for any orientation of the inducing magnetic field.9,10 Therefore, not at all surprisingly, although the work of synthesis was very recent,1 a theoretical paper elucidating the current pathways in infinitene has already appeared11 when our article was still in progress. In that work it has been clearly shown that the induced current is characterized by two aromatic, non-intersecting global π-electron current pathways, formed by the two circuits of 24 carbon atoms along the edges shaped as...
the infinite symbol. This finding answers the first three of the above questions. In addition, it addresses the question of whether the molecule follows Hückel $4\pi + 2$ or Möbius $4\pi$ aromaticity rules, showing that nitrene does not belong to any of these classes of molecules. Nonetheless, the last three questions remain. It is the purpose of this article to elucidate these additional aspects.

## METHODS

We have taken the geometry of the $(P,P)$-isomer of nitrene, optimized at the PBE0/6-311+G(d,p) level of theory in the gas phase, reported by Krzeszewski et al.\(^1\) The symmetry point group of the structure is $D_2$ with the Cartesian $x$-axis perpendicular to the central C–C bonds of the stacked naphthalene subunits, as shown in Figure 1. Then, we have performed the calculation of the magnetically induced current density using the CTOCD-DZ method to ensure origin-independent results,\(^12\) adopting the B97-2 (ref 13)/6-311+G-(2d,p) (ref 14) level of theory in the gas phase. The Gaussian 16 program\(^15\) was used to obtain the perturbed molecular orbitals, spanning the symmetries $\Gamma = \text{⊕} \text{⊕} \text{⊕} \text{⊕}$ and 24 more orbitals that can be tentatively classified as $\pi$ orbitals

$$\Gamma_\pi = 6A \oplus 5B_1 \oplus 6B_2 \oplus 7B_1$$

Using some facilities contained in the SYMOIC package, we have readily identified the set composed by HOMO, HOMO $-$ 1, HOMO $-$ 2, ..., HOMO $-$ 14 plus HOMO $-$ 17 as nearly true $\pi$ orbitals, as confirmed by inspection with GaussView. Searching for the remaining eight orbitals was revealed to be unsuccessful due to large $\sigma/\pi$ mixing. Then, only HOMO, ..., HOMO $-$ 14 plus HOMO $-$ 17 have been used in the calculation of the current density map induced in the $\pi$-electron cloud. The calculated CTOCD-DZ $\pi$-electron current density, induced by a unitary magnetic field parallel to the Cartesian $x$-axis, is shown in Figure 1. Considering that the typical benzene ring current has a maximum value of about 0.08 au,\(^17\) we have applied a lower/higher cutoff of 0.05/0.1 au to the current density values calculated over a grid of $12 \times 20 \times 28 \ \alpha_0$ in steps of 0.4 $\alpha_0$. As can be observed, the result is impressively clear and in full agreement with the current pathways reported in ref 11. Two distinct current flows can be seen to occur along the equivalent circuits of 24 carbon atoms, each one formed by all the $K$-regions of a coronene subunit plus the internal fjord region of the second coronene subunit. Looking carefully, the two global ring currents are really disjointed, as already noted, since along the radial bond of the coronene subunits the current goes in opposite directions. As can be observed, the homotropicity of the current pathways is a direct consequence of the magnetic group of symmetry,\(^18\) which can be worked out according to Tavger and Zaitsev.\(^19\) Actually, when the magnetic field is parallel to $C_2$, the magnetic group is $D_2(C_2) = (EC_2 RC_2 RC_2)$, where $R$ is the time reversal operator. Every symmetry element can be easily seen looking at the current density field depicted in Figure 1.

This qualitative result is confirmed by the quantitative representation given by the calculated all-electron bond...
current strengths reported in the bottom panel of Figure 2. The two panels in the top of Figure 2 have been calculated separating the contribution given by the set of 16 orbitals identified as nearly true $\pi$ orbitals (top left) and the contribution given by all the remaining 140 orbitals (top right), which includes also the eight orbitals showing large $\sigma/\pi$ mixing. What is shown in the top right panel of Figure 2 can be due to delocalized currents coming from $\sigma$ electrons, which are known to be somewhat less than 10% of the total current in benzene, but also due to the residual $\sigma/\pi$ mixing. At any rate, in the bottom panel of Figure 2 a real representation is given of the current delocalization, which is not affected by any ambiguous assumption. As can be observed, the current strength along the terminal K-regions is about 92% of the benzene current strength; it increases in the intermediate K-regions and reaches a maximum of 111% within the fjord regions. The current strength for the radial bonds of the coronene subunits is vanishing for all those bonds which are interchanged by $C_2$ symmetry elements and is not larger than 0.5 nA/T in all other cases. This shows quantitatively the disconnection of the two global ring currents. The apparent lack of current conservation is due to currents which do not follow the bond skeleton, but go through space, as already reported in ref 11. In particular, we have found that these through-space currents follow the trajectories of the molecular graph that is obtained by the topological analysis of the electron density gradient, shown in Figure 3. As can be observed, six bond critical points (BCPs) plus seven ring critical points (RCPs) are detected within the space between the two helices. BCPs are found exactly midway each pair of unbounded carbon atoms having the shorter distances, i.e., the two pairs formed by the central carbon atoms of the stacked naphthalene subunits, which are at 2.954 Å far apart, and the other four around these central pairs as shown in Figure 3, for which the C–C distance is 2.978 Å. Similar bond paths have been previously reported for helicenes. The two carbon atoms of each pair are connected by a bond path (shown as magenta lines) corresponding to the trajectories of $\nabla \rho$, leaving the BCP along the direction of the positive eigenvector of the
HOMO and A, respectively, while the symmetries of the HOMO, B₁; a full set of transitions active for both translation and rotation arise from these few orbitals. Remarkably, these through-space currents stem from the orbitals considered above furnish a diatropic portion and a paratropic portion, which coincide with the diatropic circulation on the rim of a coronene subunit and the paratropic circulation on the hub of the other subunit; see in Figure 2 blue/red numbers for diatropic/paratropic. Notably, the current strength diatropic/paratropic ratio is reversed with respect to pristine coronene, where the current strength on the rim is 3 times larger than that on the hub. This has a consequence on the computed magnetizability, whose component \( \xi_{xx} \) in infinite nitene is \( -812 \) cgs ppm (continuous set of gauge transformations (CSTG) method), which is much less than 2 times \( \xi_{xx} \) in infinite benzene (same method). Let us expand the topic in a more formal way, assuming the conventional correlation that links linearly the diamagnetic exaltation \( \Lambda \) to the magnetic anisotropy \( \Delta \xi \). According to such a convention, the bigger \( |\Delta \xi| \) is, the bigger \( \Lambda \) will be. Molecular magnetizability components for the main principal axes \( K_x, K_y, \) and \( K_z \) are collected in Table 1, along with those of the reference compounds coronene and benzene, calculated by using the same CSGT/B97-2/6-311+G(2d,1p) method for all molecules. Here, \( K_z \) is used to indicate the component parallel to the main symmetry axis in benzene and coronene, while it indicates the component parallel to the \( C_2 \) symmetry axis of infinite nitene. Then, the anisotropy is calculated as

\[
\Delta \xi = K_z - \frac{1}{2}(K_x + K_y)
\]  

(3)

Remarkably, it turns out that the anisotropy of infinite nitene is fairly less than those expected for an aromatic compound.
Indeed, in comparison to coronene, for which $\Delta \xi$ is calculated to be more than 7 times the anisotropy of benzene (in this case the rim current strength is remarkably high), infinitene shows a $\Delta \xi$ that is only 8.8 times the benzene anisotropy. This result is easily understood on the basis of the current density strengths reported in Figure 2; i.e., the two paratropic islands reduce $\Lambda$ in relation to their surface. Roughly speaking, one can consider 12 times the benzene anisotropy as expected for the anisotropy of infinitene, being 12 the number of benzene rings forming the molecule, minus 2 paratropic rings for the fjord regions, minus some more effects due to nonplanarity, to arrive at the 8.8 ratio. In these terms we estimate a $\Lambda$ reduced to 73% of the value expected for a planar stripe of benzene molecules.

1H NMR Chemical Shifts. The experimental 1H NMR spectrum of infinitene presents six doublet peaks within the aromatic region (from 6.4 to 8.2 ppm) which have been successfully assigned to the various kinds of protons on the basis of a very good comparison with calculated chemical shifts at the GIAO-DFT/B3LYP/6-311+G(2d,p) level of theory in CHCl$_3$ with an SMD solvent model. It was suggested that it is reasonable to attribute the larger shielding of the protons attached to the central naphthalene (H$_4$ and H$_6$, same labeling as in ref 1) to an effect from the ring current on a lower benzene ring. No other argument was given supporting this idea. Given the particular form of the magnetically induced current density, i.e., there are no ring currents localized on benzene rings, we have considered that a different explanation could exist.

To see that, we have computed the spatial contributions to the 1H NMR magnetic shieldings, at the CSGT/B97-2/6-311+G(2d,p) level, using the method proposed by Jinger et al. For the application of this method, integration of the magnetic shielding density function has to be performed adopting Becke’s partition scheme for the calculation of molecular integrals. Due to the fairly high sensitivity of the atomic contributions on the atomic size adjustments chosen to decompose the molecular space, the BCP positions of the electron density gradient have been used to define the heteronuclear cutoff profiles.

In planar aromatics the out-of-plane component of the nuclear magnetic shielding tensor is the one of major interest. Owing to the disjointed global current density induced by a magnetic field parallel to the $x$ direction, as discussed above, a similar importance is expected to occur for the $xx$ component of the tensor. Therefore, we have focused our attention on both the $xx$ and isotropic components of the proton magnetic shieldings.

Results are assembled in Figure 5 formed by six panels, one for each symmetry unique proton of the molecule (same labeling as in ref 1). In each panel, contributions to the $xx$ component of the tensor are plotted on the left beside the contributions to the isotropic component (tensor average value) on the right. Spatial contributions are represented as spheres of radii proportional to the cubic roots of the calculated values and centered on the corresponding nuclei. Shielding/deshielding contributions are shown in red/blue.

According to the Biot–Savart law the current effect decreases with the square of the distance. Moreover, closed current loops around atomic nuclei or centered on chemical bonds that do not cover the reference position provide negligible effects irrespective of their strength. Following this key of interpretation, common to all protons it can be seen that

(i) A main shielding contribution (core contribution) is given by the molecular region around each proton.

(ii) The nearest atoms provide the next important contributions.

(iii) Sizable contributions come from atoms at intermediate distances, or even far away, as a consequence of the globally delocalized current.

(iv) The contribution given by the bonded carbon atom to the $xx$ component of the magnetic shielding is always negative (deshielding), which turns always positive (shielding) for the isotropic component.

(v) Large deshielding contributions from the next-nearest atoms are negative to both $xx$ and isotropic components.

(vi) With the exception of the attached carbon atom and some very minor ones, the isotropic contributions closely resemble the $xx$ contributions, revealing the dominant role played by the delocalized current, even if moderated to some extent by the perpendicular components.

Going into details, it can be observed that all pictures for protons H$_c$, H$_d$, H$_e$, and H$_f$ (see middle and bottom rows of

Figure 5. Spatial contributions to the proton magnetic shieldings. See text for details.
Figure 5) show similar features. For H_b there are larger contributions coming from lower benzene rings. For H_c, the picture is completely different, showing important deshielding contributions from the carbon atoms forming the fjord region plus a crown of shielding contributions all along the rim of the coronene subunit in which the proton is inserted.

To deal with such a tangled situation, we have collected in Table 2 the core contribution and the sum of all shielding contributions (SSSC), Sum of Deshielding Spatial Contributions (SDSC), and Proton Net Charges q_i.

Table 2. Contributions to the Isotropic Component of the Proton Magnetic Shieldings: Core, Sum of Shielding Spatial Contributions (SSSC), Sum of Deshielding Spatial Contributions (SDSC), and Proton Net Charges q_i

| proton | SSSC | SDSC | total | δ_expt | q_i   |
|--------|------|------|-------|--------|-------|
| H_a    | 18.85| 8.91 | 27.76 | 7.14   | 6.99  | 0.1675 |
| H_b    | 19.83| 6.95 | 26.78 | 6.44   | 6.43  | 0.1320 |
| H_c    | 19.76| 5.79 | 25.55 | 7.62   | 7.60  | 0.1387 |
| H_d    | 19.79| 5.49 | 25.28 | 8.08   | 8.04  | 0.1385 |
| H_e    | 19.76| 5.36 | 25.12 | 8.24   | 8.18  | 0.1398 |
| H_f    | 19.78| 5.25 | 25.03 | 8.22   | 8.16  | 0.1433 |

(positive) and deshielding (negative) spatial contributions to the isotropic component of the magnetic shielding of the infinitene protons. Total values have also been transformed in calculated chemical shifts δ_cal relative to TMS using:

\[ δ = \sigma_{\text{ref}} - σ_i + δ_{\text{ref}} \]  

(4)

where σ_ref is the computed shielding constant for the same nucleus in a reference compound, σ_i is the computed shielding constant for the nucleus in the molecule of interest, and δ_{ref} is the experimental chemical shift for the reference compound relative to TMS. For aromatic protons we use C₆H₆ as the reference compound, adopting δ_{ref} = 7.36 ppm in CdCl₄.  

First of all, we remark the good comparison with experimental chemical shifts: the order of the signals is correctly computed and the largest deviation is only 0.15 ppm for H_f.

Looking at the core contributions, it can be observed that protons c, d, e, and f show almost the same value (maximum deviation 0.03 ppm), indicating a very similar internal region. The same protons display a decreasing sum of shielding spatial contributions (SSSC) going from H_d to H_f (Δσ = 0.54 ppm) in parallel with a decreasing sum of deshielding spatial contributions (SDSC); H_d deviates a little from this tendency. This behavior changes a lot for H_a and H_b. The latter shows an SSSC equal to 6.95 ppm, which surpasses by 1.16 ppm the value relative to H_a accounting quantitatively for the δ_{exp}(H_a) = δ_{exp}(H_f) = 1.17 ppm. This increment of the SSSC can be traced back to the somewhat larger shielding contributions from the carbon atoms of the lower benzene rings and from the K-regions of the coronene subunit, visible on the right in the top row in Figure 5. With regard to H_f everything is changed: the core contribution is the smallest, while in absolute value both the SSSC and the SDSC are the largest. This leads to cross compensations, which collocate the H_f chemical shift midway between H_a and H_b. Looking at Figure 5, top row on the left, it is possible to locate the source of the largest deshielding on the carbon atoms forming the fjord and the source of the largest shielding on the carbons in the lower benzene rings and K-regions as well. In other words, seen along the x-axis, H_f is inside two counterrotating currents and undergoes their opposite effects, i.e., the paratropic one giving a deshielding effect and the diatropic one giving a shielding effect. The smaller core contribution can be attributed to a loss of electron charge in the intimate region around the nucleus, which is compatible with the calculated Mulliken populations, showing that the four H’s have the highest positive charge within the set of hydrogen atoms. It is known that, upon formation of CH–π interactions, the hydrogen loses electrons. In our case (Figure 3) there is no bond path between the hydrogen and carbon atoms of the above ring. However, the C–C bond path is curved toward the hydrogen, indicating that the hydrogen is involved in this interaction.

CONCLUSIONS

Returning to the unsolved questions underlined before for infinitene, we have shown the following: (iv) As for the strength of the current, induced by a perturbing magnetic field perpendicular to the central C–C bonds of the two stacked naphthalene subunits, in the K-regions it is 1.5 times weaker than the diatropic current that circulates on pristine coronene rim, while in the fjord the current is 2 times stronger than the paratropic current on pristine coronene hub. (v) The exaltation of diamagnetism is fairly low, being only 73% of the expected value. (vi) The high-field ¹H NMR signals are due to the global currents flowing on the fjord region and on the carbon atoms on the lower benzene rings and K-edges, with a fairly large deshielding effect on H_a, the former, and shielding effects on both H_a and H_b, the latter.

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Notes

The authors declare no competing financial interest.

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