Observations of Low-frequency Radio Emission from Millisecond Pulsars and Multipath Propagation in the Interstellar Medium

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Abstract

Studying the gravitational-wave sky with pulsar timing arrays (PTAs) is a key science goal for the Square Kilometre Array (SKA) and its Pathfinder telescopes. With current PTAs reaching sub-microsecond timing precision, making accurate measurements of interstellar propagation effects and mitigating them effectively has become increasingly important to realize PTA goals. As these effects are much stronger at longer wavelengths, low-frequency observations are most appealing for characterizing the interstellar medium (ISM) along the sightlines toward PTA pulsars. The Murchison Widefield Array (MWA) and the Engineering Development Array (EDA), which utilizes MWA technologies, present promising opportunities for undertaking such studies, particularly for PTA pulsars located in the southern sky. Such pulsars are also the prime targets for PTA efforts planned with the South African MeerKAT, and eventually with the SKA. In this paper we report on observations of two bright southern millisecond pulsars, PSR J0437–4715 and PSR J2145–0750, made with these facilities; MWA observations sampled multiple frequencies across the 80–250 MHz frequency range, while the EDA provided direct-sampled baseband data to yield a large instantaneous usable bandwidth of ∼200 MHz. Using these exploratory observations, we investigate various aspects relating to pulsar emission and ISM properties, such as spectral evolution of the mean pulse shape, scintillation as a function of frequency, chromaticity in interstellar dispersion, and flux density spectra at low frequencies. Systematic and regular monitoring observations will help ascertain the role of low-frequency measurements in PTA experiments, while simultaneously providing a detailed characterization of the ISM toward the pulsars, which will be useful in devising optimal observing strategies for future PTA experiments.

Key words: instrumentation: interferometers – ISM: general – methods: observational – pulsars: general – pulsars: individual (PSR J0437–4715, PSR J2145–0750)

1. Introduction

The detection of nanohertz gravitational waves is the primary science goal for current and future pulsar timing arrays (PTAs; van Haasteren et al. 2011; Demorest et al. 2013; Manchester et al. 2013; Janssen et al. 2015; Bailes et al. 2018). Success in this area will extend the spectrum of gravitational-wave (GW) astronomy, opened up by recent LIGO detections of stellar-mass black hole and neutron-star merger events (Abbott et al. 2016, 2017), to frequencies where binary supermassive black holes are expected to dominate (Sazhin 1978; Detweiler 1979). With PTAs around the world achieving sub-microsecond or better timing precision, it has become important to carefully assess various contributing factors to the noise budget in timing data. These include the jitter noise arising from intrinsic pulsar emission processes that give rise to temporal variations of pulse shape or structure (e.g., Olsowski et al. 2011; Shannon et al. 2014; Lam et al. 2016), delays and distortions to pulsar signals caused by interstellar propagation effects (e.g., Cordes & Shannon 2010; Levin et al. 2016), and possible bias or uncertainties arising from instrumental effects, including calibration and data processing (e.g., van Straten 2013; Foster et al. 2015). Of these, the investigation of interstellar medium (ISM) effects has become a subject of considerable attention over recent years, since they may give rise to perturbations in timing measurements on timescales of approximately months to years, which can potentially result in low-frequency noise that can either mask or subdue the GW signatures in PTA measurements.

The magnitudes of ISM effects are strong functions of the observing frequency, $f$. For example, the dispersion delay due to propagation through cold plasma scales as $f^{-2}$, whereas pulse broadening due to multipath scattering inherent to propagation through turbulent plasma scales as $f^{-4}$ (e.g., Bhat et al. 2004). Therefore, in the early days of PTA efforts, it was thought that ISM effects, particularly time-varying dispersion...
measure (DM), can be well modeled and corrected for using observational data that span well-separated frequencies (e.g., Manchester et al. 2013). Further, it was also thought that effects of multipath scattering may not be a major concern for most PTA pulsars, given their low to moderate dispersion measures (DM $\lesssim 50$ pc cm$^{-3}$). However, recent investigations have significantly changed such a perception. For instance, from an observational perspective, applying DM corrections has proven more difficult than previously thought (e.g., Keith et al. 2013; Lee et al. 2014; Jones et al. 2017). Moreover, phenomena such as extreme scattering events have been seen even in PTA data (e.g., Coles et al. 2015; Kerr et al. 2018).

There has also been a surge of theoretical efforts aimed at understanding more subtle effects caused by the ISM, for example, chromatic dispersion that can arise owing to the frequency dependence of ISM propagation paths or volumes sampled (Cordes et al. 2016). The work of Lam et al. (2015) highlighted the need to develop observing strategies that optimally sample temporal variations of dispersion. Such strategies may also be pulsar dependent, since the nature of the ISM can vary significantly between different sight lines. Further, the advent of wide-band instrumentation stimulated the investigation of developing optimal methods and strategies that allow the determination of pulse arrival times by taking into account the frequency evolution of pulse profiles over large bandwidths. This can also potentially enable more effective DM corrections (Liu et al. 2014; Pennucci et al. 2014; Lentati et al. 2017). However, owing to chromatic dispersion, correcting high-frequency dispersive delays using low-frequency observations may not be straightforward (Cordes et al. 2016; Shannon & Cordes 2017).

These recent studies have shown that applying ISM corrections to PTA measurements is more complex than previously thought. Even though ISM effects can, in principle, be alleviated by resorting to shorter-wavelength observations ($\gtrsim 3$ GHz; Shannon et al. 2015), this is currently not a feasible option for the majority of PTA pulsars, at least within the sensitivity limitations of current facilities. Moreover, current PTA limits are largely dictated by a small number of well-timed pulsars (Lentati et al. 2015; Shannon et al. 2015; Arzoumanian et al. 2018), and therefore detailed observational investigations of ISM effects can prove to be highly instructive. Applying whatever possible corrections, or even eliminating or deprioritizing targets for which effective ISM corrections prove difficult, may help converge on more optimal observing strategies for future PTAs. A detailed characterization of the ISM along the sight lines toward PTA pulsars would serve as a logical first step in that direction, for which observations at low frequencies are highly appealing.

Over the past decade, a suite of new low-frequency facilities have become available for pulsar science: the Murchison Widefield Array (MWA) in Western Australia (Tingay et al. 2013), the Long Wavelength Array (LWA) in the United States (Taylor et al. 2012), and the Low Frequency Array (LOFAR) in the Netherlands (van Haarlem et al. 2013), all operating at frequencies below $\sim 300$ MHz. The MWA is also an official Precursor for the low-frequency component of the Square Kilometre Array (SKA-Low). Furthermore, the use of MWA Precursor technologies has led to the construction of the Engineering Development Array (EDA; Wayth et al. 2017)—a 35 m SKA-Low station equivalent built out of MWA dipole elements. Both are located in the shire of Murchison, where SKA-Low will be built. Therefore, notwithstanding their current limitations in achievable sensitivities, the MWA and EDA offer promising avenues for exploratory ISM studies of southern PTA pulsars, which will also be the prime targets for PTAs planned with the South African MeerKAT (Bailes et al. 2018), and eventually with the SKA (Janssen et al. 2015). The MWA has also been upgraded with the addition of 128 new tiles (Phase II), and extending maximum baselines out to $\sim 6$ km (R. B. Wayth et al. 2018, in preparation). The MWA and EDA allow pulsar observations at frequencies from 50 to 300 MHz and can be exploited for a wide range of studies relating to pulsar emission physics and probing the ISM.

In this paper, we report on some early observational science that leverages the large fractional bandwidths provided by the MWA and EDA. The focus of this paper is on the two brightest millisecond pulsars (MSPs) in the southern sky, PSR J0437−4715 and PSR J2145−0750, which can be studied with both of these instruments. The combination of the MWA and EDA facilities has enabled their detections down to $\sim 50$ MHz. Observational data spanning such large fractional bandwidths are particularly useful for detailed low-frequency characterization, including profile and scintillation studies. In Section 2 we give a brief overview of the facilities used, with details on observations and data processing summarized in Sections 3 and 4. Our main results are described in Section 5, and further discussion and future work are summarized in Section 6. Our conclusions are presented in Section 7.

## 2. Facilities

### 2.1. The MWA

The MWA, originally conceived primarily as an imaging telescope, has been adapted to function also as a pulsar-capable facility through the integration of a voltage capture system (VCS) that follows the second-stage polychannel filter bank (Tremblay et al. 2015). This voltage capture functionality allows the recording of $24 \times 1.28$ MHz from 128 tiles (where each tile is a $4 \times 4$ dipole array), in both polarizations, at the native 100 $\mu$s, 10 kHz resolutions. The data rates are, however, large, i.e., 7.78 GB s$^{-1}$ or approximately 28 TB hr$^{-1}$, and the system is capable of recording a maximum duration of $\sim 90$ minutes at a given time. Because the MWA’s hybrid correlator (Ord et al. 2015) was designed to generate visibilities at a rate no faster than once every 500 ms, the VCS capability has become the primary mode of observing pulsars and fast transients. The recorded data are transported to the Pawsey Supercomputing Center, where they can be run through various post-processing pipelines.

Even though the maximum recordable bandwidth of the VCS is limited to 30.72 MHz, the flexible design of the MWA receiver and the signal path (Prabu et al. 2015) can be exploited to leverage the large fractional bandwidth provided by the MWA by distributing the maximum recordable bandwidth into multiple smaller sub-bands (each 1.28 MHz wide) so as to sample multiple frequencies simultaneously, e.g., $24 \times 1.28$ MHz channels at $\sim 10$ MHz separations to cover the nominal 70–300 MHz operating frequency range. This allows simultaneous observations at multiple different frequencies across the MWA’s band, which is useful for a range of science goals, e.g., exploring the spectral evolution of the pulsar emission and investigating the frequency dependence of ISM effects such as dispersion and scattering.
2.1.1. The MWA Upgrade

Observational data presented in this paper were obtained during 2016–2017, when the MWA underwent a major upgrade, which involved the deployment and commissioning of 128 new tiles, effectively expanding on the original array, i.e., the Phase I MWA. Of the newly added tiles, 72 are configured into $2 \times 36$ hexagonal layouts (each termed a “Hex”) to provide a large number of redundant baselines, while the remaining 56 are placed farther out from the original array to provide longer baselines up to $\sim 6$ km (i.e., doubling of the imaging resolution and reducing the confusion limit). The basic system architecture, in terms of ability to correlate or voltage-record, is, however, limited to a maximum of 128 tiles at a given time. An important feature is that the array can be periodically reconfigured either as a compact array, in which the majority of the 128 tiles are located within a central region 300 m across (comprising the two Hex’s and the core), or as an extended array that includes 56 outer tiles and some fraction of the core. These new capabilities are formally referred to as the Phase II MWA.

Even though the equivalent collecting area, or the achievable sensitivity, remains essentially the same as far as pulsar observations are concerned, calibration and beam-forming with the compact configuration will naturally be far less susceptible to potential residual errors from ionospheric calibration.\textsuperscript{12} Such a compact configuration is also extremely appealing for undertaking large-area pulsar surveys given the significant reduction in the computational cost for realizing beam-forming across (or pixelizing) the full field of view (FOV).

2.2. The EDA

The EDA is effectively an implementation of the SKA station concept using MWA-style precursor technology. Details on its design, construction, and commissioning are described in Wayth et al. (2017). It is an SKA-Low station equivalent built from 256 MWA dipoles configured to work as a phased array $\sim 35$ m in size. The facility is located at the Murchison Radio-astronomy Observatory and is hosted by the MWA under its external instrument policy.\textsuperscript{13} The antenna elements are standard MWA dipoles with a low-noise amplifier design modified to extend the frequency coverage down to $\sim 50$ MHz. A phased-array mode is realized through two stages of analog beam-forming in the signal path; in the first stage, each group of 16 dipoles is connected to a standard MWA analog beam-former, and hence 16 beam-formers service the 256 dipoles that make up the array. The signals from these 16 beam-formers are then connected via 200 m coaxial cables to a beam-former controller unit in a radio frequency (RF) shielded hut, where they are combined in the second-stage beam-former, after appropriate delays, to make a phased-array signal from the entire array. The data acquisition system then captures raw baseband data over the full 327.68 MHz band and can record this on to disks. The pointing ability of the EDA is currently limited by the maximum delay possible in the MWA beam-former, and the array layout is such that each group of 16 dipoles makes a subarray of $\sim 10$ m in size, which limits the maximum zenith angle (ZA) to $25^\circ$ (i.e., a decl. coverage from the equator to $\sim 50^\circ$ south).

Even though the EDA was primarily built for prototyping and verification purposes relating to SKA-Low development, we have been able to effectively turn it into a pulsar-capable facility by integrating a pulsar processing pipeline to operate on the beam-formed voltage time series generated. This allows observations to be made over a large instantaneous bandwidth of $\sim 50$–300 MHz. Furthermore, even with its limited pointing capability, pulsars such as PSR J0437$-$4715 and PSR J2145$-$0750 can still be observed, albeit for fairly short durations of $5$–10 minutes on a given day.\textsuperscript{14} While this is indeed a limitation, the timing stability of the EDA has been pleasingly good, and we have been able to synchronously combine data from multiple observations spanning up to several months, to yield good-quality pulsar detections.

3. Observations

Observations of PSR J0437$-$4715 and PSR J2145$-$0750 were made with the MWA and the EDA; the details are summarized in Tables 1 and 2. Observations with the MWA made use of both the Phase I and Phase II array configurations, the latter being in the compact configuration comprising the two Hex’s and the core to provide a 128-tile array with a 300 m extent. VCS recording was made in two different modes: (i) over a contiguous band of 30.72 MHz bandwidth ($24 \times 1.28$ MHz) to enable high-quality profile and scintillation studies, and (ii) by distributing the 30.72 MHz bandwidth into multiple smaller units and spacing them out to span a larger frequency range, thereby effectively realizing simultaneous multifrequency observations across the MWA’s 70–300 MHz frequency range. The latter allows, in effect, sampling a large frequency span, but at the expense of reduced sensitivity (per contiguous sub-band), and is particularly suited for studies of profile evolution across the MWA band and for high-precision DM determinations. Both these capabilities are relatively new and mark significant improvements over our early work (e.g., Bhat et al., 2014, 2016). For each pulsar, data were recorded over durations of 30–60 minutes, i.e., $\sim 14$–28 TB per observation. Details on data processing procedures are summarized in Section 4.1.1.

In the case of the EDA, its limited pointing capability and the available computational resources for data processing (for performing phase-coherent de-dispersion over a large bandwidth) restricted our data recording to fairly short observations on a given day (typically $\sim 300$ s). The data rate is comparatively modest (4-bit samples, two polarizations, at the Nyquist rate of 655.36 MB s$^{-1}$), and the typical observation results in $\sim 200$ GB. Early test observations were made on 12 December 2016 (PSR J0437$-$4715), and following the successful integration of the DSPSR pipeline (van Straten & Bailes 2011) for processing EDA data streams, further observations were made during 2017 April–December (see Table 2 for details). Multiple observations were made of both PSR J0437$-$4715 and PSR J2145$-$0750 and were combined later for improved detections. The details on data processing are briefly outlined in Section 4.1.2.

\textsuperscript{12} In some rare cases, the achievable sensitivity may also be a function of the (synthesized) beam size, e.g., for observations of the Crab, the nebular emission is resolved with $\sim 5$ km baselines of the extended Phase II array, resulting in increased sensitivity.

\textsuperscript{13} http://www.mwatelescope.org/images/documents/2012.07.25_MWA_external_instruments_policy_approved.pdf

\textsuperscript{14} Longer observations are possible, albeit at the expense of reduced sensitivity, as a subset of dipoles will no longer be pointed toward the pulsar. In practice, the main limitations are the resources available for data acquisition and processing.
4. Data Processing

The high time resolution data provided by the MWA and EDA signal paths are fundamentally different and therefore require different processing pipelines for generating beam-formed time series at high time and frequency resolutions that are most amenable for pulsar detections. We briefly describe the basic steps in generating such time series data and the methods we employ for their flux calibration. Further details including calibration for full polarimetry will be detailed in an upcoming paper.

4.1. Generation of Beam-formed Time Series

4.1.1. The MWA

VCS-recorded data can be coherently summed to generate a tied-array (phased-array) beam on the sky by performing a coherent addition of voltage signals from individual tiles (S. M. Ord et al. 2018, in preparation). This maximizes the achievable sensitivity and is thus the preferred mode for pulsar observations with the MWA. However, this procedure involves incorporating polarimetric beam responses of individual tiles (using analytic models for the beams), as well as the cable and geometric delay models and complex gain information (amplitude and phase) for each tile. The calibration can make use of an in-field bright source, or multiple moderately bright sources in the field, or sometimes pointed observations of one of the bright calibrators (e.g., Hydra A, 3C 444, Hercules A) taken prior to pulsar observations. In all these cases, first the visibilities are created using the MWA correlator (Ord et al. 2015), and then for each sub-band a calibration solution (for both amplitude and phase) is iteratively generated for each tile using the Real Time System (RTS; Mitchell et al. 2008).

The output from the RTS is a calibration solution for each coarse channel, i.e., 24 solutions per observation for each tile. Between iterations, tiles with poor-quality calibration solutions are flagged out (the number tends to vary depending on the observation). Once solutions have converged for each sub-band, a coherent tied-array beam is produced using only those tiles with good solutions. The full processing chain runs on the Galaxy cluster of the Pawsey supercomputing facility and is routinely employed for sensitive pulsar observations (e.g., McSweeney et al. 2017; Meyers et al. 2017).

There is, however, an important caveat associated with the choice of the in-field calibration strategy. Since the tile (primary) beam pattern is a strong function of the observing frequency, if the calibrator is not in close proximity to the pulsar, it may lead to difficulties calibrating higher-frequency bands as the calibrator becomes near (or outside) the edge of the beam (and hence not ideal for reliable calibration). For example, Pictor A, which is located at \( \sim 10^6 \) from the position of PSR J0437−4715, is no longer a suitable in-field calibrator for this pulsar at frequencies \( \gapprox 220 \) MHz. Observations across the full MWA band may therefore warrant considering additional (or alternate) strategies to ensure successful calibration across the full frequency range.

4.1.2. The EDA

The output of the second-stage beam-former in the EDA signal path is low-pass filtered and sampled at a rate of 655.36 MHz. For pulsar observations, the resultant data streams are rescaled to 4-bit samples before writing out to disks as a dual-polarization voltage time series. These data can therefore be processed using the phase-coherent dispersion removal technique over the majority of the 327.68 MHz band, enabling pulsar observations over a large instantaneous bandwidth. In practice, the available bandwidth is limited by the response range of MWA dipoles (i.e., \( \sim 50–300 \) MHz) and the rapid growth of dispersive delay at low radio frequencies. The DSpsr software package,\(^\text{15}\) which has been the backbone of multiple generations of pulsar back ends at the Parkes 64 m telescope, has been integrated with the output of the EDA data stream. The baseband data stream can be coherently de-dispersed while dividing the full EDA band into sub-bands (typically 32k channels) using the convolving filter bank (van Straten & Bailes 2011) to generate virtually artifact-free pulse profiles. For a given DM, the lowest radio frequency amenable to coherent de-dispersion depends on the computational memory available for processing.

4.2. Flux Density Calibration

The MWA and EDA are promising instruments for investigating the low-frequency regime of flux density spectra. However, such aperture array instruments require suitably devised approaches for calibrating pulsar flux densities. Below we describe the methods employed for the initial studies presented in this paper.

4.2.1. MWA Detections

Flux calibration for MWA pulsar detections made use of the technique developed by Meyers et al. (2017). In summary, we simulated the tied-array (phased-array) beam pattern by modeling it as the product of the tile beam pattern and the array factor (see their Equations (11) and (12)). The tile beam pattern was simulated using the formalism as per Sutinjo et al. (2015), and the array factor depends on the configuration used.

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\(^{15}\) [http://dspsr.sourceforge.net](http://dspsr.sourceforge.net)
for the observation (i.e., whether Phase I or Phase II, and the number of tiles used to form a tied-array beam on the pulsar). The simulated tied-array beam is then convolved with the global sky model (de Oliveira-Costa et al. 2008) and integrated over the sky (see Sokolowski et al. 2015) to produce estimates of the antenna temperature $T_{\text{ant}}$. These are then used to calculate the system temperature $T_{\text{sys}}$, under the assumption that the radiation efficiency $\eta_{\text{rad}} \approx 1$ and using the receiver temperature measurements ($T_{\text{rcv}} \approx 40$ K) for the MWA. The integral of this array factor power pattern is then used to determine the beam solid angle $A_e$ from which the tied-array gain $G = A_e / 2k_B$ (where $A_e$ is the effective collecting area and $k_B$ is the Boltzmann constant) is estimated and translated into the system equivalent flux density $\text{SEFD} = T_{\text{sys}} / G$. Using this approach, we estimated $G$ and $T_{\text{sys}}$ for each sub-band of observations across the MWA band, by factoring in also the directional and frequency dependencies of the MWA tile pattern. We then use the standard radiometer equation for pulsar observations (i.e., accounting for the pulsar duty cycle $W/P$, where $W$ is the equivalent pulse width and $P$ is the pulsar period) to calculate the corresponding flux density scales for our observations (Lorimer & Kramer 2004). The equivalent width $W$ is estimated as $A_{\text{pulse}} / S_{\text{peak}}$, where $A_{\text{pulse}}$ is the integrated flux within the “on” pulse region and $S_{\text{peak}}$ is the peak amplitude of the detected pulse. These are then used to estimate the flux density scales at multiple frequency bands of MWA observations.

4.2.2. EDA Detections

As described in Wayth et al. (2017), the performance of the EDA is well characterized, particularly in terms of the receiver and system temperatures, the beam and sky models, and the sensitivity. Further, as shown in their Figure 9, the predicted sensitivity based on the beam and sky models is found to be in good agreement with measurements. Therefore, it is justifiable to use the EDA beam model to calculate the effective collecting area $A_e$ and the system temperature $T_{\text{sys}}$, and consequently, the sensitivity $A_e / T_{\text{sys}}$, or $\text{SEFD} = 2k_B T_{\text{sys}} / A_e$, for the specific pointing directions of PSR J0437–4715 and PSR J2145–0750. The system temperature $T_{\text{sys}} \approx \eta_{\text{rad}} T_{\text{ant}} + T_{\text{rcv}}$, where $T_{\text{rcv}}$ is the receiver temperature and $T_{\text{ant}}$ is the antenna temperature, calculated as the beam-weighted average sky temperature, using the well-known sky model of Haslam et al. (1982) at 408 MHz (see Equation (3) in Wayth et al. 2017), scaled to the observing frequency as $T(f) = T_{408}(f_{408}/f)^{\beta}$, where $\beta = -2.55$, $f_{408}$ is the frequency (in MHz), and $T_{408}$ is the sky temperature at 408 MHz. As all our EDA observations were made near the meridian transit, this provides fairly reliable estimates of the sensitivity. The values of $G$ and $T_{\text{sys}}$ obtained in this manner are then used to estimate the flux density scales at multiple frequency bands of EDA observations (i.e., in 5.12 MHz sub-bands, across the EDA band), in a manner similar to that for MWA pulsar detections (see Section 4.2.1).16

5. Analysis and Results

In this paper we limit the analysis to some basic properties that can be gleaned using the current capabilities of the MWA and EDA, specifically, pulsar detections in total intensity at frequencies spanning the 50–250 MHz range and scintillation studies that are possible with the 10 kHz spectral resolution of the VCS. More detailed analysis, e.g., full polarimetric profiles, variability in DM, and scintillation from an ongoing monitoring project, will be reported in a future paper. Even these exploratory observations provide useful insights into aspects such as the spectral evolution of the mean pulse profile and scintillation properties. We also measure pulsar flux densities to investigate the spectral behavior at low frequencies; however, we caution that robust estimates will require data from multiple observations over long time spans, in order to average over variations caused by refractive modulation.

5.1. Pulse Profiles

Pulsar detections from our observations are summarized in Figures 1–5. In Figures 1 and 3 we present MWA detections at multiple frequencies, along with those at higher frequencies (from Parkes), to illustrate the evolution in the mean pulse profile with frequency. MWA data are not coherently de-dispersed,17 and therefore they are subject to residual dispersive smearing within the 10 kHz channel width. The resultant temporal smearing is relatively small (i.e., less than the 100 $\mu$s native resolution of VCS) at frequencies down to 130 MHz for PSR J0437–4715, and down to 195 MHz for PSR J2145–0750; however, it becomes quite substantial at lower frequency bands: ~0.5 ms at the lowest frequency bands of our detections, i.e., at 81 MHz for PSR J0437–4715 and at 111 MHz for PSR J2145–0750.

For PSR J2145–0750, de-dispersion using the catalog DM of 8.998 pc cm$^{-3}$ results in a visible phase shift of approximately 0.11 phase turns across our 110–220 MHz range (see Figure 2). We therefore determined the DM from our own observations using the PDMP utility of the parfile package. Our measured DM = 9.004 ± 0.003 pc cm$^{-3}$ is significantly larger than the catalog value, and the implied DM excess ($\delta$DM = 0.006 pc cm$^{-3}$) is in close agreement with that reported by Dowell et al. (2013) from their LWA observations at frequencies below 100 MHz. We then reprocessed our data at this refined DM. We note, however, that this excess is several times larger than the maximum DM variation of

16 We exclude the sub-bands in which no meaningful detections were made, or those severely corrupted by radio frequency interference.
17 The tied-array beam output is currently written out as full Stokes PSRFITS, the capability to generate higher time resolution voltage time series is under development.
0.001 pc cm\(^{-3}\) that is reported from the 6 yr span of Parkes PTA data (Keith et al. 2013). Such a DM excess at low frequencies can possibly be attributed to chromatic DM, as theorized by Cordes et al. (2016), but we defer further discussion on this topic until Section 5.3.

EDA data were coherently de-dispersed using the DSPSR software package. Given the computational constraints of the processing machine (32 GB of RAM), the data were processed using the convolving filter bank to simultaneously coherently de-disperse the signal while dividing the 327.68 MHz baseband stream into \(32,768 \times 10\) kHz channels. This provides an effective time resolution of 100 \(\mu\)s, which is also the native time resolution of VCS data, and thus can facilitate meaningful comparison of pulse profiles. With a collecting area equivalent to 16 MWA tiles (i.e., 1/8 of the full array), the EDA is less sensitive (per unit bandwidth); however, it offers the advantage of obtaining virtually artifact-free pulse profiles. Our EDA detections of PSR J0437–4715 and PSR J2145-0750 are shown in Figures 4 and 5 at frequencies in the 50–210 MHz range.

Figure 5 shows pulse profiles of PSR J0437–4715 at frequencies 64 to 131 MHz, where the pulsar was comparatively weaker at frequencies \(\lesssim 200\) MHz in this observation.

5.1.1. Frequency Evolution

MSPs generally show complex pulse profiles, with a large number of components, unlike most normal pulsars (e.g., Dai et al. 2015). The degree of complexity often extends to polarization properties, including highly complex polarization position angle variations across the pulse phase, which cannot be well described by the rotating vector model (e.g., Xilouris et al. 1998). Moreover, the emission is often seen to extend over a significant fraction of the pulsar period (\(W_{10} \gtrsim 0.5P\), where \(W_{10}\) is the width of the pulse measured at 10% of the peak flux, and \(P\) is the rotation period). Furthermore, the conventional radius-to-frequency mapping (Komesaroff et al. 1970; Cordes 1978), which often manifests as a considerable narrowing of the pulse with an increase in the observing frequency, is seldom seen with MSPs (e.g., Kramer et al. 1998). Overall, MSP profiles have been quite challenging to model in terms of emission geometries, which may be due to multiple emission regions within the magnetosphere and pulse components originating at different locations (see Gil & Krawczyk 1997; Kramer et al. 1998; Xilouris et al. 1998; Dyks et al. 2010).

The recent work of Dai et al. (2015) has been very instructive in understanding the frequency evolution of MSP profiles. Using 6 yr of PTA data from Parkes, they were able to...
perform phase-resolved spectral studies of MSP emission properties, including polarization variations across the pulse phase. PSR J0437–4715 is known to exhibit rather complex, and quite remarkable, evolution in its mean pulse shape (e.g., Navarro et al. 1997; Bhat et al. 2014). Further, as noted by Dai et al. (2015), the profile features in their high-quality Parkes data are generally consistent with our published MWA observations (at a frequency of ∼200 MHz), where a central bright component is flanked by multiple outer components (see Figure 1). Parkes data at very high signal-to-noise ratios (S/Ns; see Figure A1 of Dai et al. 2015) also reveal the emission extending out to more than 85% of the pulse period (i.e., ∼300° in longitude), which was first reported by Yan et al. (2011; though also seen by Navarro et al. 1997). This is now also seen in our very high quality MWA detection (S/N ∼ 3400) shown in Figure 1 (the right panel), where the detectable emission extends to approximately 75% of the pulse period (i.e., ∼260° in longitude).

A comparison of MWA and Parkes data shows that the profile evolution of this pulsar is largely due to its highly complex spectral index (α) variation across the pulse. As seen from the work of Dai et al. (2015), α varies from −0.8 to −2.2 across the large emission window; while the leftward outer-edge component has a relatively flatter spectrum (α > −1.5), the emission within a ∼0.2 phase range left of the central component shows a relatively steeper spectrum (−1.7 > α > −2.2). The emission within a ∼0.2 phase range right of the central component shows a more complex variation, whereby α varies from −1 to −2.2 rather smoothly, and is marked by two prominent minima and maxima. As seen from Figure A1 in Dai et al. (2015), the leading and trailing outer components have generally steeper spectra, which may explain their rapid evolution at the MWA’s frequencies.

The pulsar profile is also known for its unusual double-“notch” feature (see Figure 1; near phase 0.075 in the 438 MHz profile), besides a notch-like feature near the center, particularly in observations at frequencies in the 0.4–1.5 GHz range (Navarro et al. 1997). It appears that the disappearance of the central notch-like feature may be due to the complex spectral index changes. For instance, the rather abrupt change of α from −2 to −1 closer to the center (i.e., near phase 0 in Dai et al. 2015) may explain the ultimate low-frequency dominance of one component and disappearance of this central notch-like feature.

The disappearance of the double-notch feature in MWA data is likely due to the limitation in our temporal resolution. The width of this feature is approximately 0.01 phase (Navarro et al. 1997), i.e., ∼50 μs, and hence as such is difficult to resolve with our 100 μs native time resolution.19 The location of this notch feature also happens to be near a local minimum in the spectral index variation, and the resulting nonuniform evolution of the components could also potentially lead to its disappearance in the MWA band. On the other hand, the leftward outer-edge region of the profile (i.e., phase <0.3 in Figure 1) exhibits a relatively flatter spectrum (α > −1.5), which may also explain its reduced prominence at the MWA’s frequencies.

PSR J2145–0750 presents yet another interesting case. As evident from Figure 3, the relative strengths of its leading and trailing components continue to decrease at lower observing frequencies and are reversed in the MWA band. Such a reversal was noted earlier by Kuzmin & Losovsky (1996) in their observations at 102 MHz, and more recently in LOFAR data reported in Kondratiev et al. (2016). This can be readily explained given the results of Dai et al. (2015), whose data we re-present in Figure 3. As can be seen from their Figure A23, the leading component of the pulse has α within the range −1.5 > α > −2, whereas for the trailing component it is −2 > α > −2.5. This readily explains the observed reversal of the relative strength and its rapid evolution within the MWA band (Figure 3, left panel). The high time resolution of Parkes data also reveals finer structure, which is not resolved in MWA observations, largely due to the limited time resolution of VCS (100 μs) and non-negligible dispersive smearing (from our 10 kHz channels). Further, the precursor component that appears at 0.2 phase offset prior to the leading peak is not seen in MWA data; this is quite perplexing considering its expected amplitude of ∼10%–40% of the leading peak, assuming the relatively steep spectral index (α ∼ −2) that was inferred by Dai et al. (2015). This may suggest either a possible turnover of the precursor emission or its plausible intermittent nature.

5.2. Scintillation

The low-frequency bands of the MWA are especially well suited for scintillation studies of low-DM pulsars such as PSR J0437–4715 and PSR J2145–0750. For instance, basic properties such as scintillation bandwidth νfl and timescale τiss can be deduced using well-established 2D autocorrelation function (ACF) analysis (e.g., Gupta et al. 1994; Bhat et al. 1999) and are useful in

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19 The temporal broadening due to scattering is expected to be negligibly small (∼1 μs) at the MWA’s 185 MHz.
estimating the integrated strength of scattering and scintillation velocities (e.g., Cordes et al. 1985; Gupta 1995). Secondary spectral analysis can sometimes lead to the detection of parabolic scintillation arcs as we reported in Bhat et al. (2016; see also Stonebring et al. 2001). Furthermore, within the constraints of our 10 kHz spectral resolution and the achievable sensitivity, it may also be possible to investigate the frequency scaling of scintillation parameters in some cases, given our multifrequency sampling across large fractional bandwidths.

5.2.1. Dynamic Spectra

The dynamic spectrum $S(f, t)$ is a 2D record of pulse intensity in time and frequency. It is the most basic observable for scintillation analysis. Figures 6 and 7 show such spectra for PSR J0437–4715 and PSR J2145–0750 obtained over 0.5–1 hr durations, over a continuous 30.72 MHz bandwidth (Figure 6), as well as 9 × 2.56 MHz bands for PSR J2145–0750 (Figure 7). Diffractive scintillation is seen as rapid, deep modulation of pulse intensity in time and frequency, whereas the drifting of intensity maxima (in the time–frequency plane) is generally attributed to refraction through the ISM. Drifting scintles can also be explained by the relative velocities of Earth and the pulsar projected onto the scattering screen; interference with the Doppler-shifted scattered radio waves causes periodic temporal variability of pulse intensity. These temporal variations give rise to drifting when combined with periodic spectral variability due to the temporal delay of the scattered rays (Walker et al. 2004). Drifting scintles are most readily seen in observations of PSR J0437–4715 (Figure 6), where the dynamic spectrum is dominated by a single bright scintle that extends over a timescale longer than our observing duration. As seen from these figures, scintles vary in their brightness, size (in both time and frequency), and orientation (i.e., drift rates); however, average properties can be meaningfully characterized by computing a 2D ACF of $S(f, t)$ in frequency and time lags: $\rho(\nu, \tau) = \langle S(f, t) S(f+\nu, t+\tau) \rangle$, where $\nu$ and $\tau$ are the frequency and time lags, respectively.

The ACFs computed in this manner are shown in the bottom panels of Figure 6. The characteristic widths in frequency and time, i.e., scintillation bandwidth $\nu_0$ and timescale $\tau_{\text{iss}}$, respectively, can be determined by fitting a 2D elliptical Gaussian function to these ACFs. Following the published literature (Gupta et al. 1994; Bhat et al. 1999; Wang et al. 2005), we fit a functional form $\rho_0(\nu, \tau) = C_0 \exp[-(C_1\nu^2 + C_2\nu\tau + C_3\tau^2)]$, to yield characteristic scales: the decorrelation bandwidth, $\nu_0 = (\ln 2/C_1)^{0.5}$, measured as the half-width at half-maximum of the correlation peak; scintillation timescale, $\tau_{\text{iss}} = (1/C_3)^{0.5}$, measured as the $1/e$ width of the correlation maximum; and the drift rate, $d\tau/d\nu = -(C_2/2C_3)$. In addition, a “drift-corrected” scintillation bandwidth can also be estimated, i.e., $\nu_{d,0} = (\ln 2)^{0.5} (C_1 - C_2^2/4C_3)^{-0.5}$, to reduce the underestimation bias resulting from significant refraction typically seen in our data. The parameters determined in this manner are tabulated in Table 3.
along with some physical properties that can be derived, namely, the mean turbulence strength $C_n^2$, the strength of scattering $u$, and the scintillation pattern speed $V_{iss}$. Further, the diffractive and refractive scattering angles ($\theta_{\text{diff}}$ and $\theta_{\text{ref}}$) can be estimated from the measurements of decorrelation bandwidth and the drift rate $dt/d\nu$, respectively, under the assumption of the thin screen scattering model, which is generally employed in the context of scintillation (see Cordes et al. 1986; Gupta et al. 1994; Bhat et al. 1999).

For PSR J0437$-$4715, we measure $\nu_0 = 1.4 \pm 0.4$ MHz,20 which is consistent with that reported in an earlier publication (Bhat et al. 2014). As we summarized in that paper, there are striking discrepancies between previously published measurements, which may be attributed to the choice of suboptimal observing parameters in much of the earlier work. The mean turbulence strength, $C_n^2 = 8 \times 10^{-5}$ m$^{-20/3}$, is the second lowest (after PSR B0950$+$08; see Phillips & Clegg 1992) measured among all known pulsars, making PSR J0437$-$4715 one of the most weakly scattered pulsars. Any timing perturbations resulting from scattering can therefore be safely ignored at its timing frequencies ($\sim$1–2 GHz).

The measured drift rate $dt/d\nu$ is almost twice as large as our previous observations and of opposite sign, though this can be attributed to time-varying refraction that is commonly seen toward many of the low-DM pulsars (Bhat et al. 1999; Wang et al. 2005).

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20 The large uncertainty is due to small-number statistics arising from our limited number of scintles (see Bhat et al. 2014).
The scintillation velocity $V_{\text{iss}}$ can be derived from the measurements of $\nu_0$ and $\tau_{\text{iss}}$, e.g., in the simplest case where the scattering medium is approximated as a thin screen located at a certain distance between the pulsar and the observer, $V_{\text{iss}}$ is given by (see Gupta et al. 1994)

$$V_{\text{iss}} = A_{\text{iss}} (\nu_0 D x)^{1/2} (\nu_{\text{obs}} \tau_{\text{iss}})^{-1},$$

(1)

where $D = D_{\text{os}} + D_{\text{ps}}$ is the pulsar distance, and $x = D_{\text{os}}/D_{\text{ps}}$, i.e., the ratio of the distances from the screen to the observer ($D_{\text{os}}$) and from the screen to the pulsar ($D_{\text{ps}}$). The constant, $A_{\text{iss}}$, relates the timescale $\tau_{\text{iss}}$ to the velocity, for which Cordes & Rickett (1998) derive a value of $2.53 \times 10^4$ km s$^{-1}$ for a Kolmogorov turbulence spectrum and homogeneously distributed medium (with $\nu_0$ in MHz, $\nu_{\text{obs}}$ in GHz, $\tau_{\text{iss}}$ in s, and $D$ in kpc), and Gupta et al. (1994) derive $A_{\text{iss}} = 3.85 \times 10^4$ km s$^{-1}$ for a single asymmetrically located thin screen (and is the value that we adopt for our estimation).

The estimated scintillation velocity $V_{\text{iss}} = 99 \pm 18$ km s$^{-1}$ (including the uncertainty in the pulsar’s distance, $D = 530 \pm 60$ pc) is three times larger than the measured proper motion of 33 km s$^{-1}$ for this pulsar (Reardon et al. 2016), which may suggest an asymmetric location for the underlying scattering screen.

5.2.2. Scintillation Arcs in PSR J0437–4715 Revisited

The 2D power spectrum of the dynamic spectrum $S(f, t)$ is referred to as the secondary spectrum, $S_2(f, t) = |S^\dagger(f, t)|^2$ (where $\dagger$ indicates 2D Fourier transform), and is a powerful technique that captures interference patterns produced by different points in the image plane (e.g., Stinebring et al. 2001; Walker et al. 2004; Cordes et al. 2006). The “fringe rates” (in time and frequency), $f_t$ and $f_\phi$, are essentially the fringe frequency and delay parameters, where $f_t$ is a measure of the differential time delay between pairs of rays, and $f_\phi$ is the temporal fringe frequency. Interference between scattered wavefronts from the origin and pairs of points along an axis in the direction of the net velocity vector $V_{\text{eff}}$ produces parabolic scintillation arcs, which can be represented by $f_\phi = \eta f_t^2$. The parabolic arcs are thus essentially a natural consequence of small-angle forward scattering. The fringe frequency and delay parameters $f_t$ and $f_\phi$ can be related to the curvature of the arc ($\eta$); following Cordes et al. (2006),

$$\eta = \frac{D s (1 - s)}{2 c V_{\text{eff}}^2 \cos^2 \theta},$$

(2)

where $D$ is the pulsar distance, $s$ is the fractional distance of the screen from the source (i.e., $s = D_{\text{ps}}/D$, and $s = 0$ at the source), $D_{\text{eff}} \equiv D s (1 - s)$ is the effective distance to the screen, and $\theta$ is the angle between the net velocity vector $V_{\text{eff}}$ and the orientation of the scattered image. The quantity $V_{\text{eff}}$ is the velocity of the point in the screen intersected by a straight line from the pulsar to the observer, and it is the weighted sum of the pulsar’s binary and proper motions ($V_{\text{bin}}$ and $V_{\text{ps}}$, respectively) and the motion of the screen and the observer ($V_{\text{scr}}$ and $V_{\text{ps, obs}}$, respectively). Its transverse component $V_{\text{eff, t}}$ (see Equation (3) in Bhat et al. 2016) determines the measured timescale $\tau_{\text{iss}}$. Thus, the measurement of $\eta$ can be used to determine the location of the scatterer, when all the contributing terms are precisely known.\(^{21}\)

\(^{21}\) In general, $s$ can be determined to within a pair of solutions; however, the degeneracy can often be resolved by making use of other measurements or constraints (e.g., estimates of $V_{\text{ps}}$ and $V_{\text{scr}}$).
In a previous publication (Bhat et al. 2016) that reported our first observations of scintillation arcs in PSR J0437−4715, we used the measurement of $\eta$ and the knowledge of the pulsar’s precise orbital and astrometric parameters, to determine the location of the underlying scatterer to be at 115 ± 3 pc. Interestingly, this was consistent with the location inferred from independent observations from Parkes made 2 weeks later at a frequency of 732 MHz.

Figure 8 shows the secondary spectrum from our new observations of PSR J0437−4715 (for the dynamic spectrum shown in Figure 6); the resolutions in fringe frequency and delay axes are 0.195 mHz and 0.195 $\mu$s, respectively (i.e., identical to those in Bhat et al. 2016). The parabolic arc features are consistently seen across different frequency segments of these new observations, albeit somewhat less prominently in the upper one-sixth of the band, where the pulsar is visibly dimmer compared to the remainder of the observing band. Furthermore, the arc feature is also visibly stronger than our previous detection, albeit more diffuse in appearance, which is reminiscent of a filled parabola (e.g., Putney & Stinebring 2006). Following a feature-extraction technique as described in Bhat et al. (2016), we compute an “arc strength” parameter $P_{\text{arc}}$, given by

$$P_{\text{arc}}(\eta) = \frac{1}{N} \sum_{i=1}^{N} S_2(\eta f_{\delta i}^2, f_{\delta i}).$$  

This method, which can be compared to the 1D generalized Hough transform, is expected to be more robust, particularly when the arc feature is limited by S/N, which is the case with our detections. The summing procedure is performed along the points of arc outside an excluded low-frequency noise region, and out to delays beyond which little power is detectable (i.e., $i = 1...N$, where $N$ corresponds to $f_{\delta i} = 20 \mu$s). Further, in order to better account for the visibly larger diffused arc feature, we consider a slightly modified parameterization for the “thickness” of the parabola, $p_d$, which is essentially the...
distance (in pixel units) from the arc curvature that is used for the computation of \( S_2 \), e.g., \( P_2 = 2 \) means that only those spectral points lying within 2 pixels of the parabola (either horizontal or vertical) are included in the sum. This is expected to yield a more robust parameterization, particularly when the arc feature is more diffuse in nature.

The right panel of Figure 8 shows our estimated \( P_{\text{arc}}(\eta) \) for the secondary spectrum shown in the left panel of this figure. The curve appears to be more broadly peaked than that of our earlier detection, despite its visibly higher degree of prominence. A closer examination of the secondary spectrum also reveals that the arc feature is more prominent in the right half. The best-fit value of the curvature of the arc \( \eta \), which corresponds to the maximum value of \( P_{\text{arc}} \), is \( \eta = 0.79 \pm 0.03 \), for the case where \( P_2 = 1.5 \); however, the estimate is somewhat more uncertain if we consider the more broadly peaked curve for \( P_2 = 2.5 \) (i.e., a thicker parabola). Nevertheless, all three curves peak at similar values of \( \eta \).

The implied distance to the screen (after accounting for the expected \( V_{\text{eff}} \) at our observing epoch; for details, see Bhat et al. 2016) is \( s = 0.26 \pm 0.02 \) (or \( 115 \pm 3 \) pc), which is in excellent agreement with our previously reported measurements. This stability of the \( \eta \) value reaffirms the presence of a compact scatterer in the line of sight to the pulsar.

As seen from Equation (2), the inferred location \( s \) depends also on the orientation \( \theta \) of the scattered image relative to \( V_{\text{eff}} \) (and is generally an unknown). However, since the 3D sky geometry of the pulsar is precisely known (van Straten et al. 2001), it is indeed possible to calculate the projection of the vector velocity \( V_{\text{eff}} \) relative to the scattering screen (assuming that it is on the plane of the sky). The effective velocity is still dominated by the proper motion of the binary system, and for the two epochs of MWA observations, incidentally, the projection angles differ by only 2°.6. Therefore, any resultant changes in \( \eta \) are not easily measurable given our uncertainties.

### 5.2.3. Frequency Scaling of Scintillation Parameters

Simultaneous multifrequency observations such as those presented in this paper can also be used, in principle, to investigate the frequency scaling of scintillation parameters. Theoretical treatments based on a Kolomogorov-type turbulence spectrum for electron density fluctuations in the ISM predict \( \nu_\delta \propto \nu^{4.4} \) and \( \tau_{\text{sc}} \propto \nu^{1.2} \) (e.g., Cordes et al. 1986). However, departures from these theoretical scalings have been seen toward a number of objects, and on a global scale, observations indicate a shallower scaling (e.g., \( \nu_\delta \propto \nu^{3.9\pm0.2} \),...
Bhat et al. 2004). An important caveat is that, at low frequencies, long-term (refractive) modulations in $v_d$ and $\tau_{\text{iss}}$ can bias the measured value at a given epoch of observation (e.g., Gupta et al. 1994; Bhat et al. 1999), and ideally observations spanning many refractive cycles are needed for a reliable estimation of the frequency scaling index.

Notwithstanding this, we attempted the related analysis using our multiband observations. PSR J0437−4715 data were not suitable for this purpose, as the expected $v_d \gtrsim 1.28$ MHz bandwidth for a large subset of our data (at frequencies $\gtrsim 150$ MHz). However, our measurement of $v_d \sim 35$ kHz for PSR J2145−0750 in the 140−170 MHz band (see Figure 6) suggests that $v_d$ is measurable within the constraints of our 10 kHz spectral resolution (and 2.56 MHz sub-bands) at frequencies $\gtrsim 140$ MHz.

Figure 7 shows the dynamic spectra from our PSR J2145−0750 observations shown in Figure 2. As seen from this figure, scintles are resolved within our observing parameters, i.e., 10 kHz $\lesssim v_d \lesssim 2.56$ MHz over the 112−220 MHz frequency range of our observation. This demonstrates the value of the MWA’s observable frequency range for studying scintillation parameters as a function of frequency. However, because of the limited S/N, a full 2D correlation analysis proved less meaningful, and we therefore adopted a relatively simpler analysis, whereby we make use of 1D cuts of the 2D ACF along $\nu = 0$ and $\tau = 0$ axes to estimate $v_d$ and $\tau_{\text{iss}}$ (by fitting for a Gaussian function).

Our estimates obtained in this manner are shown in Figure 9, and the derived scaling indices are $2.3 \pm 0.3$ for $v_d$ and $0.5 \pm 0.3$ for $\tau_{\text{iss}}$, i.e., much shallower than we expect based on the empirically determined scaling or the theoretical predictions. However, this is perhaps less surprising, as our estimates are derived from a single epoch of observations and the refractive modulation may not necessarily be correlated across our large fractional bandwidth. This is probably best alleviated by multiple similar observations that span a large number of refractive cycles and by employing more optimal observing strategies (e.g., fewer sub-bands with larger sub-bandwidth to allow 2D correlation analysis and more reliable estimates).

5.2.4. Sparseness in Dynamic Spectra

The dynamic spectra of PSR J2145−0750 in Figure 7 are marked by a visible sparseness in the distribution of scintles. This time–frequency occupancy of bright features is likely related to the filling fraction, $f_d$, typically used in the context of scintillation in order to account for the density (or a finite number) of scintles in the dynamic spectrum. In the strong scattering regime, bright features are expected as a natural consequence of an exponential distribution of intensity variations, with separations in time and frequency much larger than the characteristic sizes of scintles (Cordes 1986). Observational estimations of scintillation parameters have adopted values in the range 0.2 $< f_d < 0.5$ (Gupta et al. 1994; Bhat et al. 1999) and so are larger than a more conservative value of 0.01 assumed by Cordes (1986). Observations show that this filling fraction tends to vary between pulsars. In order to quantify this time–frequency occupancy of scintles in our data, we introduce the following “sparseness” parameter:

$$s_d = \frac{1}{N_t} \sum_{i=1}^{N_t} \sum_{j=1}^{N_s} s_{\text{on}}(f_i, t_j),$$

with

$$s_{\text{on}}(f_i, t_j) = \begin{cases} 1 & \text{if } S(f_i, t_j) > 5 \sigma_{\text{off}}(f_i, t_j), \\ 0 & \text{otherwise} \end{cases}$$

where $\sigma_{\text{off}}(f_i, t_j)$ is the off-pulse rms corresponding to the dynamic spectral point $S(f_i, t_j)$. In other words, this represents the conservative case, where at least one sample within the on-pulse window contributing to $S(f_i, t_j)$ exceeds 5$\sigma$ above the mean off-pulse level (and hence some detectable pulse energy). In some ways, this can be treated as an upper limit to the filling fraction.

For PSR J2145−0750 data shown in Figure 7, values of the $s_d$ parameter computed in this manner range from $\sim 0.05$ to $\sim 0.12$, the lower values being measured for the highest two frequency bands. It is possible that the relatively low S/Ns of these data may be somewhat biasing the estimation of $s_d$. However, for the data shown in Figure 6, which are limited neither by S/N nor by small-number statistics in terms of the number of scintles, the above estimation still yields $s_d \sim 0.09$.23 This is comparable to the values for the data shown in Figure 7 and is significantly lower than that estimated for the dynamic spectra of PSR J0437−4715 in Figure 6, for which we estimate $s_d \sim 0.58$. It is possible that such low levels of time–frequency occupancy in terms of scintles are a

Table 3

| PSR      | $v_d$ (MHz) | $\tau_{\text{iss}}$ (s) | $d\nu/dv$ (MHz−1) | $V_{\text{ox}}$ (km s$^{-1}$) | $V_{\text{r}}$ (km s$^{-1}$) | $C_{\alpha}^2$ (m$^{-3}$/s$^{3/2}$) | $\theta_{\text{off}}$ (mas) | $|\theta_{\text{off}}|$ (mas) | $s_d$ |
|----------|-------------|--------------------------|--------------------|------------------------------|-----------------------------|-------------------------------|--------------------------|--------------------------|------|
| J0437−4715 | 1.43 ± 0.4  | 613 ± 165                | −181               | 114 ± 36                     | 100                         | 8 $\times$ 10$^{-5}$                  | 0.8                      | 0.2                      | 0.58 |
| J2145−0750 | 0.027 ± 0.004 | 300 ± 45                | 1080               | 99 ± 18                      | 33                          | 1.4 $\times$ 10$^{-4}$                  | 3                       | 0.2                      | 0.09 |

Note. $s_d$: The sparseness parameter that quantifies the time–frequency occupancy of scintles (see the text for details).

Table 4

| PSR      | $\alpha_c$ | $\alpha_m$ | $\alpha_p$ |
|----------|------------|------------|------------|
| J0437−4715 | −1.1 ± 0.1 | −1.41 ± 0.14 | −1.67 ± 0.04 |
| J2145−0750 | −1.73 ± 0.07 | −2.12 ± 0.07 | −1.96 ± 0.05 |

Note. $\alpha_c$: using EDA data and the measurements from Parkes; $\alpha_m$: using MWA data and the measurements from Parkes; $\alpha_p$: Parkes measurements (i.e., the mean values of $\alpha_c$ and $\alpha_m$ from Dai et al. 2015).
Figure 8. Left: secondary spectrum of PSR J0437–4715 from the MWA observations shown in Figure 8(a); the resolutions in the conjugate time (Doppler frequency) and conjugate frequency (delay) axes are 0.195 mHz and 0.195 μs, respectively. The dashed red curve indicates the best-fit curvature estimated for the arc feature (see the text for details). Right: mean arc strength $P_{\text{arc}}$ against the curvature parameter $\eta_t$ computed for different thickness parameter ($\delta_t$) of the parabolic curve. The dashed horizontal line corresponds to 1σ below the maximum value of $P_{\text{arc}}$ (for the 2-pixel curve), where $\sigma$ is computed based on the noise statistics estimated for a secondary spectral segment that is well outside the visible arc feature (see the text for details), whereas the dotted vertical lines correspond to the $\eta$ values where $P_{\text{arc}}$ is 1σ below the peak.

Figure 9. Plots of scintillation bandwidth ($\nu_{\text{d}}$) and scintillation timescale ($\tau_{\text{sc}}$) for PSR J2145–0750 at multiple frequencies within the MWA band. The uncertainties are due to the limited number of scintles, assuming a filling fraction $f_s = 0.5$. The suggested scaling indices (i.e., the slopes of the best-fit lines) are $2.3 \pm 0.3$ for $\nu_{\text{d}}$ and $0.5 \pm 0.3$ for $\tau_{\text{sc}}$.

5.3. Chromaticity in Dispersion Measure

The size of the scattering disk is $\sim D_{\text{eff}} \theta_{\text{diff}}$, where $\theta_{\text{diff}} \propto \lambda^2$; thus, the sampled ISM volume critically depends on the observing frequency $f$ (or the wavelength $\lambda$). This means substantially different propagation paths for scattered rays, which may give rise to frequency-dependent (chromatic) DMs. This idea was explored in detail by Cordes et al. (2016), who caution against the use of low-frequency observations for correcting DM variations. The importance of chromatic DMs thus crucially depends on the degree of scattering and therefore can be highly dependent on line of sight.

As discussed in Section 5.1 (see also Figure 2), processing PSR J2145–0750 data at the cataloged DM results in a striking phase shift of 0.11 turns across our MWA observing band of 110–220 MHz. It is clear that this cannot be attributed to profile evolution and implies an excess DM of 0.006 pc cm$^{-3}$. This value is several times larger than the peak-to-peak DM variation seen for this pulsar in 6 yr of PTA observations (Keith et al. 2013) and may be due to chromatic DM (Cordes et al. 2016). A similar excess was seen in initial LWA observations of this pulsar (Dowell et al. 2013) and also in ongoing monitoring observations with LWA1, which yields a typical DM of 9.0045 pc cm$^{-3}$ (K. Stovall 2018, private communication). Indeed, the ISM sampled by MWA observations would be $50–100$ times larger than that sampled by observations at timing frequencies ($\sim 1$–2 GHz), and it is even larger in the LWA observations. The observation of a similar excess in both cases suggests that this is likely a characteristic of the pulsar’s line of sight.

It is, however, possible that there may still be some (small) contribution to the observed DM excess that arises from the frequency evolution of the pulse profile, which is significant for PSR J2145–0750 (Figure 3). Assuming temporal stability of the pulse profiles, this would in principle imply a nonvariable contribution to $\delta$DM, which can be disentangled if multiple observations are made over a long enough time span. While our limited observational data do not allow us to get a handle on that, evidence in support of a persistent excess DM is also characteristic of certain lines of sight, where underlying small-scale density structures deviate from the standard Kolmogorov-type distribution. A more quantitative analysis is deferred to a future paper as further observations accrue from our ongoing monitoring project.
hinted at by our multiple observations made with the EDA over a period of ~4 months (Figure 4). A DM excess of similar magnitude is consistently seen in all observations; reprocessing EDA data at this refined DM results in nearly aligned pulse profiles across the EDA band, as seen in Figure 4. A closer examination of EDA observations also suggests that the variable component of the DM (over a 4-month time span) is of the order of ~0.001 pc cm^{-3}; more observational data are needed for a better (and more robust) estimate.

5.4. Flux Densities and Spectra

Pulsars are generally steep-spectrum radio emitters, and the studies based on large samples have shown that the spectral index varies over a large range. The measured values for the mean spectral index \( \langle \alpha \rangle \) vary from \(-1.4 \pm 0.2\) to \(-1.8 \pm 0.2\) (e.g., Maron et al. 2000; Bates et al. 2013; Jankowski et al. 2018). The spectral behavior at frequencies \( \lesssim 300 \text{ MHz} \) is poorly explored for a large fraction of the known pulsar population, particularly for MSPs, many of which were discovered and studied exclusively at higher frequencies. Low-frequency spectral studies are also complicated by substantial flux variability (by a factor of ~3–5) that arises from long-term refractive modulations (e.g., Gupta et al. 1994; Bhat et al. 1999; Wang et al. 2005). The large frequency span achievable with the MWA and the large fractional bandwidth of the EDA are promising for useful spectral studies, especially for southern MSPs, for which the spectrum at frequencies \( \lesssim 700 \text{ MHz} \) is poorly constrained (Dai et al. 2015).

5.4.1. Spectral Behavior at Low Frequencies

Using the procedures detailed in Section 4.2, we estimated the flux density measurements for the data presented in this paper. Since our MWA data are limited in both S/N and temporal resolution (besides multiple caveats of insufficient averaging of flux modulations due to scintillation effects), we limit ourselves to a fairly simple analysis, where we ignore the spectral index variation across the pulse profile, and consider just the spectrum of the average emission (i.e., integrated pulse profiles as a whole). Figure 10 presents our measured flux densities for PSR J0437–4715 and PSR J2145–0750, along with the published values from Dai et al. (2015) and Dowell et al. (2013). Parkes measurements are from regularly sampled Parkes PTA data over a 6 yr time span and therefore are more reliable; however, we note that both pulsars are seen to be highly variable even in the Parkes bands, e.g., rms variability ~50%–70% is noted for PSR J0437–4715, whereas PSR J2145–0750 is seen to vary much more, with rms variation comparable to mean flux densities in the 50 and 10 cm data (i.e., 732 MHz and 1.4 GHz). Similarly, large variations are also seen in our MWA observations, and therefore the implied spectral behavior can be considered only indicative. EDA measurements are more reliable than those from the MWA, as they are obtained from multiple observations spanning several months; for PSR J2145–0750, nine observations over a 4-month time span were used, whereas six observations spanning ~8 months were used in the case of PSR J0437–4715. Still, this only sparsely samples long-term refractive cycles, and an insufficient averaging of resultant modulations in flux densities can potentially skew our estimates. Table 4 presents a summary of our spectral index estimates.

For PSR J2145–0750, excluding LWA measurements, the combination of EDA and Parkes measurements yields a spectral index estimate, \( \alpha_e = -1.73 \pm 0.07 \); however, a larger value of \( \alpha_m = -2.12 \pm 0.07 \) is estimated if we use MWA measurements instead. The reported value of \( \alpha_p = -1.96 \pm 0.06 \) by Dai et al. (2015) is still within this range and agrees with our estimates at the 2\( \sigma \) level, which is encouraging and reaffirms a generally steeper spectrum of this pulsar. Furthermore, it appears that our measurements (in particular, those from the EDA) are not consistent with a suggested spectral turnover for this pulsar by Dowell et al. (2013). In fact, their quoted flux densities are based on a limited number of observations and hence are subject to possible bias from insufficient averaging of long-term refractive modulations, a caveat also applicable for MWA and EDA measurements. Therefore, the possibility of temporal variations (in flux densities) causing the observed inconsistency cannot be precluded.

For PSR J0437–4715, a number of factors prevented us from obtaining reliable estimates of its flux densities. It was difficult to accurately calibrate MWA observations shown in Figure 1 for reliable flux scales because a large number of tiles (58 out of 128) were flagged during the calibration procedure. The measurements shown in Figure 10 are hence from observations shown in Figure 6(a) (i.e., over 140–170 MHz, broken up into 12 × 2.56 MHz contiguous bands). Furthermore, this pulsar also shows substantial variability in apparent brightness—as much as by a factor of ~6 between different observations. Given these, the indicated \( \alpha_e = -1.1 \pm 0.07 \) (from EDA and Parkes data), which is obtained by excluding the observing epochs when the pulsar was significantly brighter than average, can only be treated as an indicative upper limit (i.e., |\( \alpha | > 1.1 \)). The spectral estimate from MWA and Parkes data is somewhat steeper (\( \alpha_m = -1.41 \pm 0.14 \)); however, it is still shallower than the value (\( \alpha_p = -1.67 \pm 0.04 \)) from Dai et al. (2015) from Parkes-only measurements. We further note that the earlier work of McConnell et al. (1996), which reported the first detection of this pulsar at frequencies below 100 MHz, was inconclusive in terms of a possible turnover at low frequencies. Further observations are needed to explore this in detail.

6. Discussion and Future Work

Using the improved capabilities of the MWA and an SKA prototyping station (the EDA) built utilizing MWA technologies, we have carried out observations of two bright southern MSPs at frequencies below 300 MHz. The primary goal was to demonstrate the advantages of large frequency spans at low radio frequencies for science relating to pulsar emission and probing ISM effects. In this paper, we have largely focused on profile evolution and scintillation studies, as well as measurements of flux densities, to investigate the nature of spectral behavior at low frequencies. Even though our analysis is based on data from a limited number of observations, it clearly demonstrates the exciting prospects for low-frequency MSP observations with the MWA and EDA facilities.

The mean pulse profiles of MSPs tend to show quite a remarkable spectral evolution. Our observations are generally consistent with the extrapolations based on the recent work of Dai et al. (2015), who performed phase-resolved spectral studies of a number of MSPs being monitored for the Parkes PTA project. Their data span the frequency range from 732 MHz to 3.1 GHz, and our observations thus extend the frequency coverage down to ~100 MHz. For PSR J2145
there is also some evidence of an excess DM, of the order of $0.006 \pm 0.003$ pc cm$^{-3}$, albeit estimated from a single observation with the MWA. This is six times larger than the peak-to-peak DM variation seen for this pulsar from a 6 yr Parkes PTA data span (Keith et al. 2013). It is, however, consistent with that inferred from low-frequency detections of this pulsar with the LWA (Dowell et al. 2013). Further, our EDA observations (over a time span of $\sim$4 months) confirm that the observed excess is persistent in the direction of this pulsar. It is possible that part of this excess DM is due to profile evolution at low frequencies, which may give rise to a fixed DM offset, assuming profile stability over time. Disentangling such a fixed DM contribution (caused by profile evolution) from a variable contribution (caused by the ISM) will require observational data spanning long time spans (months to years), sampled fairly regularly (at a weekly or monthly cadence).

A similar caveat is also relevant for our flux density and spectral index estimates. While we have been able to meaningfully flux-calibrate our pulsar detections, considering the large flux modulations that are typical at low frequencies (due to refractive scintillation), reliable flux density estimates require multiple observations spanning many refractive cycles (typically $\sim$days to weeks for low-DM pulsars). Notwithstanding this caveat, our data are in general agreement with steeper spectra for MSPs and are consistent with the recent work of Dai et al. (2015). It appears that a spectral turnover, if at all present, may be occurring at frequencies below the MWA band. This is encouraging, particularly when considering low-frequency surveys to find MSPs. The ongoing low-frequency pulsar surveys, such as the Green Bank Northern Celestial Cap survey (Stovall et al. 2014) and the LOFAR survey (Bassa et al. 2017), are already finding MSPs at impressive rates, which is consistent with the lack of evidence for spectral turnover in our observations.

In addition to mean flux densities, scintillation properties are also expected to show significant modulations at low frequencies (e.g., Gupta et al. 1994; Bhat et al. 1999). The degree of modulation is expected to be large (as much as $\sim$3–5) in the case of low- to moderate-DM pulsars, which constitute the majority of PTA pulsar samples. Recent work by Levin et al. (2016) using wide-band observations of northern PTA pulsars confirms that this is generally the case, even at frequencies $\geq$1 GHz (see also Wang et al. 2005). Hence, in order to meaningfully characterize scintillation effects, observations need to be sampled over multiple refractive cycles, the timescales of which are also longer at low frequencies (weeks to months). A strategy of this kind has also been advocated by

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Figure 10. Flux density measurements of PSR J0437$-$4715 and PSR J2145$-$0750 at frequencies spanning from 30 MHz to 3 GHz. Top panels: EDA and MWA measurements of PSR J0437$-$4715 along with Parkes (PKS) measurements; bottom panels: EDA and MWA measurements of PSR J2145$-$0750 along with LWA and Parkes measurements. LWA data are from Dowell et al. (2013), whereas Parkes measurements are from Dai et al. (2015) and are more reliable, as they are obtained from a 6 yr data span. EDA measurements are averaged over multiple observations spanning several months (see Table 2). The best-fit spectral index estimates are summarized in Table 4.
Lam et al. (2015) in the context of applying more effective DM corrections using contemporaneous observations.

In summary, there is quite a compelling case to consider routine observations of MSPs at low frequencies, particularly for PTA pulsars, whose DM and scintillation properties and temporal variabilities will be instructive in ascertaining the ISM noise budget in timing measurements. However, currently the MWA’s ability for monitoring purpose is limited by VCS recording, whose data rates and transport logistics constrain observations to a maximum 1.5 hr once every 2–3 days. However, the large FOV of the MWA can be well exploited for monitoring multiple PTA pulsars at once, e.g., at a frequency of 150 MHz (FOV \(\sim 450 \text{deg}^2\)), up to approximately five to six pulsars are covered in a single VCS pointing, thereby yielding high observing efficiency compared to all other currently operational telescopes. Such observations are under way, where the current focus is a modest sample of high-priority southern PTA pulsars.

In the near-term future, substantial improvements are being planned to enhance the pulsar capabilities of the MWA. These include the ability to reprocess the data by performing an inversion of the polyphase filter bank operation prior to the VCS recording, to yield voltage time series data at a much higher time resolution (and hence more amenable for phase-coherent de-dispersion). This will yield even higher-quality pulse profiles for MSPs. The EDA pulsar capability can also be leveraged for robust cross-checks toward verifying the coherent de-dispersion functionality for VCS data. The commissioning and verification of polarimetric capability is also under way and will enable phase-resolved spectral and polarimetric studies of MSPs, similar to the recent work of Noutsos et al. (2015) at low frequencies and Dai et al. (2015) at higher frequencies. Furthermore, as more observations accrue from our ongoing monitoring campaign, it will also become possible to undertake a more systematic investigation of subtle effects such as chromatic DM and its relevance for PTA pulsars, as well as MSP spectral behavior at low frequencies. If MSP spectra turn out to be steeper down to low frequencies, it will strengthen the case to consider low-frequency surveys to find MSPs. Such surveys will be particularly sensitive to finding pulsars with low to moderate DMs, which are most suited for PTA experiments. This will especially benefit future PTA efforts planned with the upcoming MeerKAT (Bailes et al. 2018), and eventually with the SKA (Janssen et al. 2015).

The ongoing developments toward further enhancing the capabilities of the MWA will bring further exciting prospects for MSP science at low frequencies. These include a wider-bandwidth correlator and beam-former, which will eliminate the need to sample the large frequency range by subdividing the 30.72 MHz recording bandwidth into smaller sub-bands. Moreover, the increased sensitivity will also help extend low-frequency characterization to a large sample of MSPs, an important exercise that will also facilitate a more effective integration of the MWA into global PTA efforts. In the longer-term future, the much higher sensitivity that will be attainable through a 256-tile MWA, as well as the observing efficiency achievable via a wide-band beam-former capability, will potentially transform the MWA into a premier low-frequency facility for high-quality science relating to MSPs.

7. Concluding Remarks

With the functionality to record voltage data and a suite of post-processing pipelines to perform associated calibration and beam-forming operations, the MWA is rapidly emerging as a promising facility for low-frequency pulsar astronomy in the southern hemisphere. The VCS data can be recorded over a maximum bandwidth of 30.72 MHz, either over a contiguous range or distributed over a larger range by flexibly subdividing into smaller units, to enable a simultaneous sampling of multiple frequencies, thus effectively providing large fractional bandwidths. This is particularly useful for studying spectral evolution of mean pulse profiles, which is quite remarkable for most MSPs. The data can also be used to investigate a range of ISM effects, including the recently theorized chromatic dispersion that arises from multipath propagation in the ISM, and characterizing the strength of turbulence and the degree of scattering in the sight lines toward pulsars. This is especially important for PTA pulsars and may help converge toward suitable targets and devising optimal observing strategies. We have demonstrated the potential in this area using the case studies of two bright southern MSPs (PSR J0437–4715 and PSR J2145–0750) with the MWA and EDA facilities.

Systematic monitoring of a large sample of MSPs will help ascertain the role of low-frequency observations for PTA efforts. This is particularly important for southern MSPs, which will also become the prime targets for future PTA experiments planned with MeerKAT and the SKA. The MWA is strategically located to undertake this important exercise, and its large FOV can be exploited for simultaneous observations of multiple PTA pulsars.

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