Effect of plasma resonances on dynamic characteristics of double graphene-layer optical modulator

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We analyze the dynamic operation of an optical modulator based on double graphene-layer(GL) structure utilizing the variation of the GL absorption due to the electrically controlled Pauli blocking effect. The developed device model yields the dependences of the modulation depth on the control voltage and the modulation frequency. The excitation of plasma oscillations in double-GL structure can result in the resonant increase of the modulation depth, when the modulation frequency approaches the plasma frequency, which corresponds to the terahertz frequency for the typical parameter values.

I. INTRODUCTION

The gapless energy spectrum of graphene layers (GLs) [1], results in the interband absorption of the electromagnetic radiation from the terahertz to ultraviolet range [2]. This opens up prospects to use graphene structures in active and passive optoelectronic devices. Novel lasers, photodetectors, modulators, and mixers have been proposed and studied [2–13] (see also the review paper [14] and references therein). Varying the controlling voltage one can effectively change the electron and hole densities and the Fermi energy and, hence, the intraband and interband absorption in GLs. An increase in the electron (hole) density increases the intraband absorption (associated with the Drude mechanism), but it decreases the interband absorption due to the Pauli blocking effect. Which mechanism dominates depends on the incident photon energy hΩ and the momentum relaxation time of electrons and holes, τ. At the frequencies of infrared and visible radiation, Ω ≫ τ⁻¹, so that the Drude absorption is weak. Even in the terahertz (THz) range, the latter inequality can be valid for high quality GLs (like those studied in Refs. [12,18]), even at room temperatures.

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In this paper, we develop a device model of a double-GL optical modulator proposed and demonstrated in Ref. [19]. In this modulator, GLs were separated by relatively thick barrier and the structure was integrated with an optical waveguide. The operation of the device under consideration is associated with the filling of GLs with electrons and holes injected from the contacts under the self-consistent electric field created by the applied voltage and the electron and hole charges in GLs. This process determines both static and dynamic characteristics of the double-GL modulator. At the non-stationary conditions, the dynamics of the electron-hole plasma in double-GL can exhibit resonant response due to the excitation of plasma oscillations similar to those well known in more traditional two-dimensional electron and hole systems [20,30]. The plasma oscillations in GL-structures also were considered previously (see, for instance, Refs. [31–35]). A resonant plasmonic THz using double-GL structures was recently studied in Ref. [36].

In this paper, we develop a device model for double-GL modulators of optical radiation and demonstrate that the resonant excitation of plasma oscillations in double-GL modulators can provide an efficient modulation of optical radiation by high frequency signals, in particular, in the THz range.

The variation of the Fermi energy in double-GL is associated with the electron and hole injection and extraction by the side contacts. Therefore, the consideration of the electron-hole plasma dynamics in double-GLs must ac-
count for the self-consistent electric field found from the solution of the hydrodynamic equations and the Poisson equation.

II. EQUATIONS OF THE MODEL

We consider the double-GL modulator reported in Ref. [10]. Its simplified structure is shown in Fig. 1(a). We assume that each GL is connected to one side contact and is isolated from the opposite contact (connected to the other GL). The voltage, $V_m$, applied between these contacts, $V_m = V_0 + \delta V_m$, where $V_0$ and $\delta V_m$ are the bias and modulation components. We set $\delta V_m(t) = \delta V_m \exp(-i \omega t)$, where $\omega$ is the modulation frequency. The latter is much smaller than the frequency of the incident optical radiation $\Omega$: $\omega \ll \Omega$. The system of two highly conducting side contacts can be considered as a slot line enabling the propagation of the modulation signals. The side contacts can also be connected to or be a part of THz antenna, which converts the incoming THz radiation into the modulation voltage.

The absorption coefficient of the light wave propagating along the waveguide with double-L on topGL is determined by the real part of the double-GL conductivity $\text{Re}\sigma = \text{Re}\sigma^{\text{intra}} + \text{Re}\sigma^{\text{inter}}$ at the frequency $\Omega$:

$$\beta_\Omega = \frac{4\pi \text{Re}(\sigma_\Omega) \Gamma_\Omega}{cv \sqrt{k}},$$

(1)

where $c$ is the speed of light in vacuum and $k$ is the dielectric constant of the waveguide material. The symbol $\langle \ldots \rangle$ means the averaging accounting for the distribution of the optical field $E_\Omega(x, y)$ in the waveguide, where the $x$-axis and $y$-axis correspond to the direction along double-GL structure and perpendicular to the $z$-axis corresponding to the direction of the wave propagation direction in the waveguide. Thus,

$$\langle \sigma_\Omega \rangle \Gamma_\Omega = \frac{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E_\Omega(x, y)|^2 dx}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E_\Omega(x, y)|^2 dx dy},$$

(2)

where

$$\Gamma_\Omega = \frac{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E_\Omega(x, y)|^2 dx}{\int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |E_\Omega(x, y)|^2 dx dy},$$

is the mode overlap factor and $2L$ is the GL length, which is approximately equal to the spacing between the side contacts as shown in Fig. 1(a).

We assume that the electron and hole momentum relaxation time is associated with the scattering due to disorder and acoustic phonons, so that its energy dependence is given by $\tau^{-1} = \nu(\varepsilon/T_0)$, where $\nu$ is the characteristic scattering frequency at $V = 0$ (at the Dirac point). In this case, the real part of the conductivity of two GLs at $\Omega \gg \nu_0$ can be presented as [10]

$$\text{Re}\sigma_\Omega = \left\{ \begin{array}{ll}
\frac{e^2}{4\hbar} & \text{for } \frac{\hbar \Omega}{2} \gg T + \mu_+ - \mu_- \\
1 + \exp\left(\frac{\hbar \Omega/2 - \mu_+}{T}\right) & \text{for } \frac{\hbar \Omega}{2} \ll T + \mu_+ - \mu_-
\end{array} \right\} - \frac{1}{1 + \exp\left(\frac{\hbar \Omega}{2} \mu_+ \right)}.$$

(3)

Here $\mu_+$ and $\mu_-$ are the GL Fermi energies counted from the Dirac point in the upper and lower GLs, respectively, $T$ is the temperature, and $e$ is the electron charge. The first five terms in Eq. (4) correspond to the contributions of the interband transitions to the conductivity of the upper and lower GLs. These terms explicitly account for the Pauli blocking effect. The last term in Eq. (3) accounts for the intraband transitions. It is presented in the form

FIG. 1: Schematic view of (a) double-GL modulator structure coupled with an optical waveguide and (b) band diagram of GLs under a voltage drop between them (shaded areas indicate the states occupied by electrons).
providing an interpolated dependence of the intraband conductivity on the Fermi energies and the temperature. At slow variation of the applied voltage, \( \mu_+ = \mu_- = \mu \), where \( \mu \) obeys the following equation:

\[
2\mu + \Delta = eV_m
\]

(4)

The quantity \( \Delta \) is determined by the electric field between GLs and the thickness of the barrier layer between GLs \( d \). Generally speaking (at sufficiently fast variations of the voltage), the spatial distributions of the electron and hole densities do not follow the variation of the applied voltage, and the Fermi energies depend on the coordinate \( x \): \( \mu_+ = \mu_+(x) \) and \( \mu_- = \mu_-(x) \).

The Fermi energies in GLs are governed by the following formulas which relate the densities \( \Sigma \) and \( \mu \),

\[
\beta_\Omega = 1 - \frac{1}{1 + \exp(\frac{h\Omega}{2T} - \sqrt{\frac{2V_m}{\nu}})} - \frac{32
\frac{\nu T}{2}}{\pi^2}\frac{V_m + \frac{\pi^2}{12}}{\nu T}
\]

(13)

Here

\[
\beta_\Omega = \frac{2\pi\alpha\Gamma_\Omega}{\sqrt{k}}
\]

(14)

\( \nu \) is the characteristic collision frequency of electrons and holes (which is assumed to be proportional to \( T \)), and \( \alpha = e^2/\hbar c \approx 1/137 \) is the fine structure constant, (so that \( \pi \alpha \approx 0.023 \)).

In the near infrared range of frequencies, \( \hbar \Omega \gg T \), the contribution of the intraband absorption at low control voltages \( V \) is small. This implies that the last term in the right-hand side of Eq. (13) is much smaller than unity.

At sufficiently large bias voltage \( V_0 \), the electron and hole systems in GLs become degenerate (i.e., \( \mu \gg T \)), and Eq. (10) yields

\[
\mu \approx T \sqrt{\frac{2V_m}{V}} = \hbar \nu V \sqrt{\frac{kV_m}{4ed}}
\]

(11)

so that, taking into account Eq. (4),

\[
\Delta \approx eV_m - 2T \sqrt{\frac{2V_m}{V}} = eV_m - h\nu V \sqrt{\frac{kV_m}{ed}}.
\]

(12)

Using Eqs. (1) and (3) and considering Eq. (8), we arrive at the following formula for the absorption coefficient:

\[
\frac{I_0}{I_{00}} = \exp\left[-\frac{\beta_\Omega H}{1 + \exp(\frac{h\Omega}{2T} - \sqrt{\frac{2V_m}{\nu}})}\right]
\]

(15)

where \( H \) is the double-GL length in the direction of radiation propagation, and \( \hbar \Omega_0 = \hbar \nu V \sqrt{kV_0/ed} \propto \sqrt{V_0} \).
Equation (15) describes the variation of the output radiation $I_0$ caused by relatively slow variations of the applied voltage $V_m$ with arbitrary swing. Using Eq. (15), one can estimate the modulation depth $m_0$ and the extinction ratio $\eta$ for the case of relatively slow modulation and when $V_m$ varies from $V_m = 0$ to $V_m = V_m^{\text{max}} > \frac{V_m^{\text{max}}}{v_W^2}$, where $\frac{V_m^{\text{max}}}{v_W^2} = \frac{4e\delta}{k} \left( \frac{\Omega}{v_W} \right)^2$: $m_0 = 1 - \exp(-\gamma H)$ and $\eta = \exp(\gamma H)$.

IV. SMALL SIGNAL LINEAR MODULATION CHARACTERISTICS

We now assume that $V_0$ is sufficiently large to form the degenerate electron and hole systems in the pertinent GLs, while the time dependence of $\delta V_m(t) \ll V_0$ is still characterized by a small modulation frequency. In this case, from Eq. (15) we obtain the following formulas of the modulation amplitude $\delta I_0$ and the modulation depth of the output radiation $\delta m_0$:

$$\frac{\delta I_0}{I_{00}} = \frac{\beta H}{\lambda} \exp\left\{ -\frac{\beta H}{\lambda} \frac{\hbar(\Omega - \Omega_0)}{2T} \right\} \left\{ 1 + \exp\left( \frac{\hbar(\Omega - \Omega_0)}{2T} \right) \right\} \frac{\delta V_m}{\sqrt{2V_0}},$$

(16)

and

$$\delta m_0 = \frac{\beta H}{\lambda} \left( \frac{2T}{\hbar(\Omega - \Omega_0)} \right) \frac{\delta V_m}{\sqrt{2V_0}},$$

(17)

where $\hbar \Omega_0 = h v_W \sqrt{kV_0/ed} \propto \sqrt{V_0}$.

In particular, at $eV_0 = \hbar \Omega_0$, when $\delta m_0$ reaches a maximum, Eqs. (16) and (17) yield respectively

$$\frac{\delta I_0}{I_{00}} = \frac{\beta H}{\lambda} \exp\left( -\frac{\beta H}{\lambda} \frac{\hbar(\Omega - \Omega_0)}{2T} \right) \frac{\delta V_m}{\sqrt{2V_0}},$$

(18)

and

$$\delta m_0 = \frac{\beta H}{\lambda} \frac{2T}{\hbar(\Omega - \Omega_0)} \frac{\delta V_m}{\sqrt{2V_0}}.$$

(19)

V. PLASMA OSCILLATIONS IN DOUBLE-GL STRUCTURES

In the double-GL structures with sufficiently high conductivity at low modulation frequencies, one can use Eq. (6), i.e., put $\varphi_{\pm} = \pm \frac{V_m}{2}$. However, at elevated modulation frequencies (for instance, in the THz range), the spatial distributions of the ac components of the electron and hole charges, the electron and hole Fermi energies, and the self-consistent electric potential are nonuniform because these distributions do not follow fast modulation signals. In sufficiently perfect GLs, the modulation signals can excite the electron-hole plasma oscillations. In this situation, the ratio of the ac component of the radiation intensity $\delta I_\omega$ to the input intensity is given by the following equation, which replaces Eq. (16):

$$\delta I_\omega = \frac{\beta H}{\lambda} \frac{2T}{\hbar(\Omega - \Omega_0)} \exp\left( -\frac{\beta H}{\lambda} \frac{\hbar(\Omega - \Omega_0)}{2T} \right) \left\{ 1 + \exp\left( \frac{\hbar(\Omega - \Omega_0)}{2T} \right) \right\} \frac{\delta V_m}{\sqrt{2V_0}} \cdot$$

(20)

The last factor in the right-hand side of Eq. (20) accounts for the contributions of different parts of GLs being dependent on local values of the Fermi energies and, hence, the local values of the ac potentials [see Fig. 1(b)].

To find the distributions of $\varphi_{\pm}$ and $\varphi_{-\pm}$, one can use a system of hydrodynamic equations (Euler equation and continuity equation) adjusted to the features of the electron and hole spectra in GLs [35] for the electron and hole plasmas in the upper and lower GLs coupled with the Poisson equation. For simplicity, we use the Poisson
The latter boundary condition reflects the fact that the electron and hole currents are equal to zero at the disconnected edges of GLs (at $x = -L$ in the upper GL and at $x = L$ in the lower GL).

First from Eqs. (21) and (22) we obtain

$$\delta \varphi_+ + \delta \varphi_- = A x,$$

(25)

where $A$ is a constant. Considering Eq. (25), Eqs. (21) and (22) can be presented as

$$\frac{d^2 \delta \varphi_+}{dx^2} + \frac{\omega (\omega + iv)}{s^2} (\delta \varphi_+ - \delta \varphi_-) = 0,$$

(26)

$$\frac{d^2 \delta \varphi_-}{dx^2} + \frac{\omega (\omega + iv)}{s^2} (\delta \varphi_- - \delta \varphi_+) = 0.$$  

(27)

Solving Eqs. (26) and (27) with boundary conditions (24) and (25), we obtain

$$\delta \varphi_+ = \frac{\delta V_m}{2} \left( \frac{\cos \gamma_\omega x}{\gamma_\omega \sin \gamma_\omega L - x} - \frac{\gamma_\omega \sin \gamma_\omega L}{\cos \gamma_\omega L - L} \right),$$

(28)

$$\delta \varphi_- = -\frac{\delta V_m}{2} \left( \frac{\cos \gamma_\omega x + x}{\gamma_\omega \sin \gamma_\omega L - x} - \frac{\gamma_\omega \sin \gamma_\omega L}{\cos \gamma_\omega L - L} \right).$$

(29)

Here $\gamma_\omega = \sqrt{2\omega (\omega + iv)/s}$. Introducing the characteristic plasma frequency $\omega_p = \pi s/2\sqrt{2L}$, one obtains $\gamma_\omega L = \pi \sqrt{\omega (\omega + iv)/2\omega_p}$.

In the low modulation frequency limit (when $\omega \ll L^2/2\pi^2 \nu = 4\omega_v^2/\pi^2 \nu = \tau_M^{-1}$, where $\tau_M^{-1}$ is the Maxwell relaxation time, and, hence, $|\gamma_\omega L| \ll 1$), one obtains $\delta \varphi_+ = \delta V_m/2$ and $\delta \varphi_- = -\delta V_m/2$, i.e., the spatial distribution of the ac potential across the GLs is flat.

Figure 2 shows examples of the spatial distributions of the amplitudes of the ac potential across GLs, calculated for different modulation frequencies using Eqs. (28) and (29). As seen from Fig. 2, the amplitudes $|\delta \varphi_+|$ and $|\delta \varphi_-|$ are close to the amplitude of the applied ac voltage $\delta V_m/2$ at relatively low modulation frequencies ($\omega/2\nu = 0.20$ and 0.5 THz). However, with increasing $\omega$, the amplitudes dramatically increase (see the curves corresponding to $\omega/2\nu = 0.80$ and 1.00 THz). This is attributed to the excitation of plasma oscillations whose amplitude grows as the modulation frequency approaches the plasma resonance frequency (see below).

VI. RESONANT MODULATION

Substituting $\delta \varphi_+$ and $\delta \varphi_-$ from Eqs. (28) and (29) into Eq. (21) and integrating over $dx$, we obtain

$$\delta m_\omega = \beta_\Omega H \frac{\exp \left[ \frac{h(\Omega - \Omega_0)}{2T} \right]}{\left\{ 1 + \exp \left[ \frac{h(\Omega - \Omega_0)}{2T} \right] \right\}^2} \frac{\sin(\gamma_\omega L)}{(\gamma_\omega L) \cos(\gamma_\omega L) - (\gamma_\omega L) \sin(\gamma_\omega L)} \frac{\delta V_m}{\sqrt{2 \nu v_0}}.$$
yielding for the normalized modulation depth:

$$\frac{\delta m_\omega}{\delta m_0} = \left| \frac{\sin(\gamma_\omega L)}{(\gamma_\omega L)[\cos(\gamma_\omega L) - (\gamma_\omega L)\sin(\gamma_\omega L)]} \right|. \quad (31)$$

Using Eq. (31), the normalized modulation depth can also be expressed via the characteristic plasma frequency $\omega_p$:

$$\frac{\delta m_\omega}{\delta m_0} = \left| \frac{\sin \left( \frac{\pi \sqrt{\omega(\omega + i\nu)}}{2\omega_p} \right)}{\cos \left( \frac{\pi \sqrt{\omega(\omega + i\nu)}}{2\omega_p} \right) - \frac{\pi \sqrt{\omega(\omega + i\nu)}}{2\omega_p} \sin \left( \frac{\pi \sqrt{\omega(\omega + i\nu)}}{2\omega_p} \right)} \right| \quad (32)$$

FIG. 3: Normalized modulation depth $\delta m_\omega/\delta m_0$ versus modulation frequency $\omega/2\pi$ for different electron and hole collision frequencies $\nu$.

At $\omega \ll \nu, \omega_p$, Eq. (32) yields

$$\frac{\delta m_\omega}{\delta m_0} \approx \left| \frac{\tan \sqrt{\omega \gamma_M}}{\sqrt{\omega \gamma_M}} \right|. \quad (33)$$

Equations (19) and (33) provide the dependences of the modulation depth on the structural parameters and the modulation frequency (particularly the frequency dependence at the roll-off) obtained experimentally and described in Ref. 19.

The character of the dependence of the modulation depth $\delta m_\omega$ on the modulation frequency $\omega$ depends on the collision frequency $\nu$. Figure 3 shows the frequency dependences (on $f = \omega/2\pi$) of the normalized modulation depth $\delta m_\omega/\delta m_0$ calculated using Eq. (32) for devices with different values of the collision frequency $\nu$. It is assumed that the plasma frequency $\omega_p/2\pi = 1.77$ THz. For the characteristic plasma velocities $s = (3.75 - 7.5) \times 10^8$ cm/s (as in the estimate in the previous section), this frequency corresponds to $2L = 0.75 - 1.5$ $\mu$m, i.e., to the length of GLs (size of the waveguide) close to the optical wavelength under consideration.

At relatively large collision frequencies $\nu$, the modulation depth $\delta m_\omega$ monotonically decreases with increasing the modulation frequency [in line with Eq. (33)]. The curve for $\nu = 10 \times 10^{12}$ s$^{-1}$ in Fig. 3 corresponds to $\tau_M \simeq 2 \times 10^{-13}$ s and the 3dB roll-off frequency $\nu_{3dB} \simeq 0.8$ THz. In the devices with a smaller $\omega_p$, i.e., with a smaller plasma-wave velocity, $s$, or larger length of GLs, $2L$, the Maxwell relaxation time is longer, so that the roll-off frequency is smaller. However, in the devices with relatively small $\nu \ll \omega_p$, $\delta m_\omega$ can exhibit a steep increase when $\omega$ approaches to the plasma resonance frequency. The sharpness of the modulation depth peak and its height rise with decreasing $\nu$ (i.e., with an increasing quality factor of the plasma resonances, $Q \sim \omega_p/\nu$). This also seen in Fig. 4 (compare the solid and dashed lines).

The plasma resonance frequencies, $\omega_n \propto \omega_p$. Here $n = 1, 2, 3, \ldots$ is the resonance index. As can be derived from Eq. (32), the resonance frequencies are given by the solution of the following equation:

$$\cot(\pi \omega_n/2\omega_p) = (\pi \omega_n/2\omega_p). \quad (34)$$

Equation (34), in particular, yields $\pi \omega_1/2\omega_p \simeq 0.86 < 1$, so that at $\omega_0/2\pi = 1.77$ THz, one obtains $\omega_1/2\pi = \ldots$
The second (even) resonance corresponds to $\omega_2/2\pi \gtrsim 3.54$ THz. Thus, apart from a pronounced first resonance, a fairly weak second resonance is also seen in Fig.3. A characteristic plasma frequency falls in the THz range. As seen in Fig. 4, an increase in $\omega_p$ and, consequently, in $\omega_n$ shifts the positions of the peaks in the frequency dependence of the modulation depth. However, this shift can not be used for the electrical control because the bias voltage $V_0$ corresponds to the energy of photons of modulated radiation. This is in contrast to other THz voltage-controlled devices using the resonant excitation of plasma oscillations (see, for instance, Ref. [36]).

VII. CONCLUSIONS

In summary, we developed a device model for an optical modulator based on the double-GL structure that was recently proposed and experimentally realized [19]. The double-GL modulator utilizes the variation of absorption due to the electrically controlled Pauli blocking effect. Our model accounts for the interband and intraband absorption and the plasma effects in GLs determining the spatio-temporal distributions of the electron and hole densities and the absorption coefficient. The developed model yields the dependence of the modulation depth on the control voltage for strong but slow modulation signals and for small-signal modulation in a wide range of frequencies. The dependence of the modulation depth on the modulation frequency is determined by the relationship between the collision frequency of electrons and holes and the characteristic plasma frequency (or between the latter and the Maxwell relaxation time). At relatively large collision frequencies (or small plasma frequencies), the modulation depth is a monotonically decreasing function of the modulation frequency. The obtained dependencies qualitatively explain the experimental results. However, we predict that in the double-GL structures with relatively weak disorder and, hence, with a low collision frequencies, and a sufficiently high quality factor of the plasma oscillations, the modulation depth exhibits a sharp maximum at the modulation frequency, which corresponds to the plasma resonance. The frequency of the latter falls in the THz range for typical parameter values. This opens up the possibility to use the double-GL structures for effective modulation of optical radiation by THz signals.

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