Transport through a strongly coupled graphene quantum dot in perpendicular magnetic field

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Abstract
We present transport measurements on a strongly coupled graphene quantum dot in a perpendicular magnetic field. The device consists of an etched single-layer graphene flake with two narrow constrictions separating a 140 nm diameter island from source and drain graphene contacts. Lateral graphene gates are used to electrostatically tune the device. Measurements of Coulomb resonances, including constriction resonances and Coulomb diamonds prove the functionality of the graphene quantum dot with a charging energy of approximately 4.5 meV. We show the evolution of Coulomb resonances as a function of perpendicular magnetic field, which provides indications of the formation of the graphene specific 0th Landau level. Finally, we demonstrate that the complex pattern superimposing the quantum dot energy spectra is due to the formation of additional localized states with increasing magnetic field.

Introduction
Graphene [1,2], a two-dimensional solid consisting of carbon atoms arranged in a honeycomb lattice has a number of unique electronic properties [3], such as the gapless linear dispersion, and the unique Landau level (LL) spectrum [4,5]. The low atomic weight of carbon and the low nuclear spin concentration, arising from the ≈99% natural abundance of 12C, promises weak spin orbit and hyperfine coupling. This makes graphene a promising material for spintronic devices [6,7] and spin-qubit based quantum computation [8-11]. Additionally, the strong suppression of electron backscattering [4,5] makes it interesting for future high mobility nanoelectronic applications in general [12,13]. Advances in fabricating graphene nanostructures have helped to overcome intrinsic difficulties in (i) creating tunneling barriers and (ii) confining electrons in bulk graphene, where transport is dominated by Klein tunneling-related phenomena [14,15]. Along this route, graphene nanoribbons [16-22] and quantum dots [23-30] have been fabricated. Coulomb blockade [23-25], quantum confinement effects [26-28] and charge detection [29] have been reported. Moreover, graphene nanostructures may allow to investigate phenomena related to massless Dirac Fermions in confined dimensions [24,31-36]. In general, the investigation of signatures of graphene-specific properties in quantum dots is of interest to understand the addition spectra, the spin states and dynamics of confined graphene quasi-particles.

Here, we report on tunneling spectroscopy (i.e. transport) measurements on a 140-nm graphene quantum dot with open barriers, which can be tuned by a number of lateral graphene gates [37]. In contrast to the measurements reported in Ref. [27] the more open dot in the present investigation enables us to observe Coulomb peaks with higher conductance and the larger dot size reduces the magnetic field required to see graphene specific signatures in the spectra. We characterize the graphene quantum dot device focusing on the quantum dot Coulomb resonances which can be distinguished from additional resonances present in the graphene tunneling barriers. We discuss the evolution of a number of Coulomb resonances in the vicinity of the charge neutrality point in a perpendicular magnetic field from the low-field regime to the regime where Landau levels are expected to form. In particular, we investigate the device characteristics at elevated perpendicular magnetic fields, where we observe the formation of multiple-dots giving rise to (highly reproducible) complex patterns in the addition spectra.

Device fabrication
The fabrication process of the presented graphene nanodevice is based on the mechanical exfoliation of...
(natural) graphite by adhesive tapes [24,25,28]. The substrate material consists of highly doped silicon (Si++) bulk material covered with 295 nm of silicon oxide (SiO2), where thickness (and roughness) of the SiO2 top layer is crucial for the Raman [38] and scanning force microscopy based identification of single-layer graphene flakes. Standard photolithography followed by metallization and lift-off is used to pattern arrays of reference alignment markers on the substrate which are later used to re-identify the locations of individual graphene flakes on the chip and to align further processing patterns. The graphene flakes are structured to submicron dimensions by electron beam lithography (EBL) and reactive ion etching based techniques to fulfill the nanodevice design requirement. After etching and removing the residual resist, the graphene nanostructures are contacted by an additional EBL step, followed by metallization and lift-off.

A scanning force microscopy image of the final device studied here is shown in Figure 1a. The approximately 140 nm diameter graphene quantum dot is connected to source (S) and drain (D) via two graphene constrictions with a width of ≈75 nm and a length of ≈25 nm, both acting as tunneling barriers. The dot and the leads can be further tuned by the highly doped silicon substrate used as a back gate (BG) and three in-plane graphene gates: the left side gate (LG), the plunger gate (PG) and the right side gate (RG). Apart from the geometry, the main difference of this sample compared to the device presented in Ref. [27] is the higher root mean square variation of the height (rh) on the island. While there are no visible resist residues on the island of the sample in Ref. [27] with rh = 0.35 nm, there are many dot-like residues on the sample presented here giving rh = 1.1 nm.

### Measurements

All measurements have been performed at a base temperature of T = 1.8 K in a variable temperature cryostat. We have measured the two-terminal conductance through the graphene quantum dot device by applying a symmetric DC bias voltage Vb while measuring the source-drain current through the quantum dot with a noise level below 10 fA. For differential conductance measurements a small AC bias, Vb,ac = 100 µV has been superimposed on Vb and the differential conductance has been measured with lock-in techniques at a frequency of 76 Hz.

In Figure 1b we show the conductance Gqd as a function of back gate voltage at low bias (Vb = 200 µV) highlighting the strong suppression of the conductance around the charge neutrality point (-5 < Vbg < 3 V) due to the so-called transport gap [19-22]. Here we tune transport from the hole to the electron regime, as illustrated by the left and the right inset in Figure 1b. The large number of resonances with amplitudes in the range of up to 0.1 e2/h inside the gap region may be due to both, (i) resonances in the graphene constrictions acting as tunneling barriers [4] (and thus being mainly responsible for the large extension of this transport gap) and (ii) Coulomb resonances of the quantum dot itself (see also examples of Coulomb diamonds in Figure 1c). At room temperature these resonances disappear and a conductance value of 0.76 e2/h is measured at Vbg = 0 V.

#### Coulomb blockade measurements at B = 0 T

By focusing on a smaller back gate voltage range within the transport gap (indicated by the dashed lines in - Figure 1b) and measuring the conductance as a function of Vbg and the right side gate Vrg much more

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**Figure 1 Device characterization.** (a) Scanning force microscopy of the graphene quantum dot device. The overall chemical potential of the device is tuned by a global back gate, where as the right side gate (RG) is used for local asymmetric tuning. The extension of the dot is around 140 nm with 75 nm wide and 25 nm long constrictions. The white dashed lines delineating the quantum dot perimeter are added for clarity. (b) Measurement of the source (S)-drain (D) conductance for varying back gate voltage showing a transport gap from around -5 to 3 V (Vb = 200 µV). (c) Coulomb diamond measurements in the gap showing a charging energy of around 4.5 meV. This energy is lower than what has been measured in an other dot of similar size (Ref. [26]), most likely because of the increased coupling to the leads. The arrows point to faint lines outside the diamonds. The extracted energy difference of around 1 meV is a reasonable addition energy for excited states. Note that for the measurement in (c), in addition to the BG the right side gate was changed according to Vrg = -0.57Vbg -1.59 V.
fine-structure appears, as shown in Figure 2. A large number of resonances is observed with sequences of diagonal lines (see white lines in Figure 2) with different slopes, corresponding to different lever arms ($\alpha$'s). By sweeping the right side gate ($V_{rg}$) we break the left-right symmetry of the transport response (see also Figure 1a). This allows us to distinguish between resonances located either near the quantum dot or the left and right constriction. The steeper the slope in Figure 2 the less this resonance can be electrostatically tuned by the right side gate and, consequently, the larger the distance between the corresponding localized state and the right side gate. Subsequently, the steepest slope (II, corresponding to $\alpha_{I} \approx 0.2$) can be attributed to resonances in the left constriction which are strongly tuned by the right side gate. In contrast resonances with lever arm (I) are only weakly affected by the right side gate and therefore attributed to states in the left constriction. The periodic resonances marked with (I) are attributed to resonances in the dot in agreement with the intermediate slope.

Coulomb resonances as a function of a perpendicular magnetic field

In Figure 3 we show a large number of Coulomb resonances as function of a magnetic field perpendicular to the graphene sample plane. The measurement shown in Figure 3a has been taken in the back gate voltage range from $V_{bg} = -5$ to -3.5 V, at $V_{rg} = 0$ V (highlighted by the horizontal line (A) in Figure 1b). Thus we are in a regime where transport is dominated by holes (i.e. we are at the left hand side of the charge neutrality point in Figure 1b), which is also confirmed by the evolution of the Coulomb resonances in the perpendicular magnetic field as shown in Figure 3a. There is a common trend of the resonances to bend towards higher energies (higher
$V_{\text{bg}}$) for increasing magnetic field, in good agreement with Refs. [27,28,32-34]. The finite magnetic field introduces an additional length scale $\ell_B = \sqrt{\hbar/eB} \approx 25\text{nm} / \sqrt{\text{T}}$ which competes with the diameter $d$ of the dot. Therefore, the ratio $d/\ell_B$ is a relevant parameter for the observation of Landau levels in graphene quantum dot devices. Here, the comparatively large size ($d \approx 140\text{ nm}$) of the dot promises an increased spectroscopy window for studying the onset and the formation of Landau levels in graphene quantum dots, where the surface-to-boundary ratio increases edge effects should be less relevant. In order to demonstrate the reproducibility of these complex patterns we show an up (Figure 3c) and a down (Figure 3d) sweep of the very same $B - V_{\text{bg}}$ parameter space. These two measurements, have different resolution and thus different sweep rates in both the $B$ and $V_{\text{bg}}$ direction. However, all the individual features are highly reproducible (but hard to understand) despite the fact that we find some small hysteresis in magnetic field for $B < 3 \text{ T}$ (see white arrows in Figure 3c, d). The origin of the complex patterns shown in Figure 3 can be understood when having a closer look at charge stability diagrams (such as Figure 2) for different magnetic fields.

In Figure 4a we show an example of a sequence of dot Coulomb resonances in the $V_{\text{fg}}-V_{\text{bg}}$ plane. The slope corresponding to $a_{\text{feg}} = 0.4$ and the spacing of $\Delta V_{\text{bg}} = 0.1$
V are in good agreement with Figure 2, and lead to the conclusion that we observe single quantum dot behaviour over a large parameter range. However, if we measure the current in the very same $V_{rg} - V_{bg}$ parameter space at $B = 7$ T the pattern changes significantly and the diagonal lines are substituted by a strong hexagonal pattern (see dashed lines) typical for two coupled quantum dots [40]. The two states forming the hexagon pattern show relative lever arms of $\alpha_{rg} \approx 0.4$ and $\alpha_{bg} \approx 1$. While the resonances with $\alpha_{bg}$ are attributed to the original dot, $\alpha_{rg}$ corresponds to a new and strongly coupled localization formed close to the right constriction. Additional resonances from the right constriction with $\alpha_{bg} \approx 1.65$ (see above) are still visible.

We interpret the magnetic field dependence in the following way. At low but increasing magnetic field we see in almost all measurements an increase of the conductance through the dot (see, e.g. Figure 3). Assuming diffusive boundary scattering such a conductance onset in magnetic field occurs due to reduced backscattering [41] and has been observed in other measurements on graphene nanoribbons [42,43]. The maximum conductance is reached around $B \approx 1.5$ T corresponding to a magnetic length $\ell_B = \sqrt{\hbar/eB} \approx 50$ nm in rough agreement with the size of the constrictions. As the magnetic field is further increased the complex pattern with many crossings starts to emerge, attributed to the formation of additional quantum dots around the right constriction with strong coupling to the original dot. The formation of such localized puddles is understood as a consequence of the increased magnetic confinement where $\ell_B$ is getting smaller than the extension of potential valleys induced by disorder.

**Conclusion**

In summary, we have presented detailed studies of transport through an open and larger graphene quantum dot (compared to Ref. [27]) in the vicinity of the charge neutrality point as a function of perpendicular magnetic field. The evolution of Coulomb resonances in a magnetic field showed the signatures of Landau level formation in the quantum dot. Indications for the crossing of filling factor $\nu = 2$ are obtained by the observation of kinks in spectral lines before bending towards the charge neutrality point. However, the observation is disturbed by the formation of a pronounced additional localized state at high magnetic fields in the vicinity of the right constriction. Although the use of open constrictions enhances the visibility of the Coulomb peaks and reduces the transport-gap region, emerging pronounced parasitic localized states make the analysis very difficult. For a further in-depth analysis of the addition spectra around the electron-hole crossover, it is hence beneficial to minimize the amount of disorder and to use clearly defined constrictions. These should be thin compared to the dot diameter to get different energy scales for quantum dot resonances and constriction resonances, which are easy to distinguish. However, the constrictions need to be wide enough to enable conductance measurements around the electron-hole crossover without a charge detector.

**Abbreviations**

BG: back gate; EBL: electron beam lithography; LL: Landau level; LG: left side gate; PG: plunger gate; RG: right side gate; SiO$_2$: silicon dioxide.

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Authors’ contributions
KE, TI, CS and JG designed the experiment. JG fabricated the sample. TF and JG carried out the transport measurements. All authors analyzed the measurements. JG and CS wrote the paper. All authors read and approved the final manuscript.

Competing interests
The authors declare that they have no competing interests.

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