THE OPTICAL LIGHT CURVES OF XTE J2123–058. III. THE MASS OF THE BINARY COMPONENTS AND THE STRUCTURE OF THE QUIESCENT ACCRETION DISK

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ABSTRACT

We present optical photometry of XTE J2123–058 taken in 1999 and 2000, during its quiescent state. The dominant feature of our R-band light curve is the ellipsoidal modulation of the secondary star; however, in order to fit this satisfactorily, we require additional components that comprise an X-ray–heated Roche lobe–filling secondary star and an accretion disk bulge, i.e., where the gas stream impacts the accretion disk. The observed dip near phase 0.8 is interpreted as the eclipse of inner parts of the accretion disk by the bulge. This scenario is highly plausible given the high binary inclination. Our fits allow us to constrain the size of the quiescent accretion disk to lie in the range (0.26–0.58)R_L1 (68% confidence). Using the distance of 9.6 kpc and the X-ray flux inferred from the heated hemisphere of the companion, we obtain an unabsorbed X-ray luminosity of $1.2 \times 10^{33}$ ergs s$^{-1}$ for XTE J2123–058 in quiescence. From the observed quiescent optical/IR colors, we find that the power-law index ($-1.4$) for the spectral distribution of the accretion disk compares well with other quiescent X-ray transients.

We also reanalyze the optical light curves of the soft X-ray transient XTE J2123–058 taken during its outburst and decay in 1998. We use a robust method to fit the data using a refined X-ray binary model. The model computes the light arising from a Roche lobe–filling star and flared accretion disk irradiated by X-rays and calculates the effects of shadowing and mutual star/disk eclipses. We obtain relatively accurate values for the binary inclination and mass ratio, which when combined with spectroscopic results obtained in Paper II, gives a neutron star mass in the range 1.04–1.56 M$_\odot$ (68% confidence).

Subject headings: accretion, accretion disks — binaries: close — stars: individual (XTE J2123–058)

1. INTRODUCTION

Soft X-ray transients (SXTs), or X-ray novae in quiescence, provide outstanding opportunities to study the mass donor and/or quiescent accretion disk in these low-mass X-ray binaries (LMXBs) because of the absence of the enormous glare that results from X-ray–heated material during outburst. The majority of these systems appear to contain black hole compact objects (Charles 2001 and references therein), but four of them have been identified with neutron stars as a result of the type I X-ray bursts seen during X-ray active phases. The rarity of neutron star transients has been explained by King, Kolb, & Burderi (1996) as due to the effects of X-ray irradiation that can stabilize the accretion disk.

Furthermore, detailed studies of many transients are hampered by galactic extinction, as most lie in or close to the Galactic plane. And, as yet, no transient has been seen to produce X-ray eclipses that would provide incontrovertible constraints on its orbital inclination. For these reasons, the recent SXT XTE J2123–058 is a system of considerable importance in this field. It is at high Galactic latitude ($b_L \sim -36^\circ 2$) and during outburst (Zurita et al. 2000, hereafter Paper I) displayed a dramatic optical modulation (the largest in this class of objects) that indicated that, even though not eclipsing, the inclination must be very high.

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Observations of type I bursts at optical (Tomsick 1998) and X-ray wavelengths (Takeshima & Strohmayer 1998) indicated that the compact object is a neutron star, making it one of only four neutron star X-ray transients.

This paper is a companion to Casares et al. (2002, hereafter Paper II) that presents the first spectroscopic detection of the companion in quiescence. Low-resolution spectroscopy of XTE J2123–058 during its quiescent state revealed a K7 V star with a radial velocity semiamplitude of $287 \pm 12$ km s$^{-1}$. Combined with the orbital period, this implies a binary mass function of $f(M) = 0.61 \pm 0.08$ M$_\odot$ (Paper II). From these, estimates of the component masses were made, but it is clear that these are limited by the accuracy of the $q$ and $i$ values.

We present the optical light curve of XTE J2123–058 taken when the source was in quiescence. We model the multicomponent optical light curves in terms of the light arising from an X-ray–heated Roche lobe–filling secondary star, the accretion disk, and the self-eclipse of the inner part of the disk by the stream/disk impact region. We also take the opportunity to reanalyze the outburst and decay optical light curves of XTE J2123–058. The model we used previously suffered from computational biases, in particular when calculating eclipses. Also, as is the case in most fitting procedures, the best-fit solution depends somewhat on the starting parameters. Here we use a genetic-type algorithm that is more robust than conventional techniques and allows us to determine accurate masses for the binary components.

2. OBSERVATIONS AND DATA REDUCTION

Cousin R-band CCD images of XTE J2123–058 in quiescence were obtained between 1999 and 2000 with the NTT
and Cousin RI observations on La Palma (see Table 1 for details). Johnson Steward Observatory, Arizona, and the WHT 4.2 m telescope on La Silla, the Bok 2.3 m telescope at the Kitt Peak National Observatory, and the INT 2.5 m telescope on La Palma (see Table 1 for details). Johnson UBV and Cousin RI observations were also obtained with the 4.2 m WHT and INT 2.5 m telescopes. In addition, infrared (JHK) observations were obtained during 1999 September–2000 June as part of the UKIRT Service Program.

All the optical images were corrected for bias and flat-fielded in the standard way. The infrared images were dark-current subtracted and then flat-fielded using a median stack of the images. We applied profile-fitting photometry to our object and several nearby comparison stars within the field of view, using IRAF. All the images were flux-calibrated except for the J-band because of the non-photometric conditions during the J-band standard star observations.

3. THE COLORS OF THE ACCRETION DISK

We use the dereddened optical and infrared colors of XTE J2123–058 to recover the broadband spectrum of the accretion disk by subtracting the companion star. We use a PHOENIX model atmosphere (Hauschildt, Allard, & Baron 1999) with \( T_{\text{eff}} = 4250 \) K and \( \log g = 4.5 \) to represent the K7 V secondary star, which is consistent with the spectral type classification by Tomisck et al. (2001). The observed mean colors and dates are given in Table 2. We first convolved the model atmosphere spectrum with the optical and infrared filter responses and then fixed the secondary star to contribute 77% of the observed flux at \( \lambda = 6300 \) Å (as determined in Paper II). By subtracting the resulting colors from the observed dereddened colors of XTE J2123–058 based on \( E_{B-V} = 0.12 \) (Hynes et al. 2001) we obtain the colors of the accretion disk (see Fig. 1). We find that the spectrum of the accretion disk can be represented as a power law of the form \( F_{\lambda} \propto \lambda^{\beta} \) with \( \beta = -1.4 \).

If we use \( T_{\text{eff}} = 4500 \) K to represent a K5 secondary star, we obtain an exponent of \(-1.1\). Changing the secondary star’s contribution to 70% increases the exponent by 0.3. Therefore, we estimate a systematic uncertainty of \( \pm 0.3 \). Since the optical and infrared observations were taken at different times, we have to assume that the mean brightness of the source does not vary with time. Ideally, we would like to determine the phase-averaged magnitudes. Although most of our measurements do not cover a complete orbital cycle, we believe that the large uncertainties in the measurement for each band are such that we allow for this systematic effect in our error estimate. The power-law index for the spectral distribution of the accretion disk compares well with that derived in other quiescent SXTs. In A0620–00 and Cen X-4, the power-law index is \(-2.5 \pm 1.0 \) (McClintock & Remillard 1986) and \(-1.6 \pm 0.3 \) (Shahbaz, Naylor, & Charles 1993), respectively.

4. A REANALYSIS OF THE OUTBURST/DECAY DATA

In this section, we re-fit the optical light curves of XTE J2123–058 presented in Paper I. The model that was originally used (Paper I) suffered from many computational biases, the result of many transfers of the code to different operating systems, which resulted in the miscalculation of eclipses. The errors in the code were noticed when we tried to produce simple images of the binary system. Also, the code was not general and could be used only for systems with relatively hot secondary stars, as is the case in high-mass X-ray binaries (Tjemkes et al. 1986), so it used Kurucz model atmospheres with temperatures hotter than 5500 K.

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**TABLE 1**

| Telescope | Date     | Exposure Time (s) | Band |
|-----------|----------|-------------------|------|
| WHT 4.2 m | 1999 Jun 28 | 7 x 530           | R    |
| WHT 4.2 m | 1999 Jul 6  | 157 x 180         | R    |
| WHT 4.2 m | 1999 Jul 7  | 1 x 600           | I    |
| WHT 4.2 m | 1999 Jul 7  | 1 x 600           | V    |
| WHT 4.2 m | 1999 Jul 7  | 1 x 1200          | B    |
| WHT 4.2 m | 1999 Jul 21 | 15 x 600          | R    |
| Bok 2.3 m | 1999 Sep 4–7| 68 x 1200         | R    |
| UKIRT 3.5 m | 1999 Sep 4 | 36 x 60           | K    |
| UKIRT 3.5 m | 1999 Sep 6 | 54 x 60           | J    |
| UKIRT 3.5 m | 1999 Sep 10| 54 x 60           | H    |
| NTT 3.5 m | 2000 Aug 27 | 39 x 600         | R    |
| INT 2.5 m | 2000 Nov 5  | 5 x 1800          | U    |
| INT 2.5 m | 2000 Nov 5  | 1 x 900           | U    |
| INT 2.5 m | 2000 Nov 5  | 1 x 600           | U    |
| INT 2.5 m | 2000 Nov 5  | 1 x 300           | U    |

**TABLE 2**

| Band | Date     | Observed Magnitude | reddening $^a$ |
|------|----------|--------------------|----------------|
| U    | 2000 Nov 5 | 23.68 ± 0.02       | 0.56           |
| B    | 1999 Jul 7  | 23.75 ± 0.11       | 0.49           |
| V    | 1999 Jul 7  | 22.65 ± 0.06       | 0.37           |
| R    | 1999 Jul 21 | 21.81 ± 0.02       | 0.27           |
| I    | 1999 Jul 7  | 21.08 ± 0.04       | 0.18           |
| H    | 1999 Sep 10 | 19.48 ± 0.49       | 0.06           |
| K    | 1999 Sep 4  | 19.98 ± 0.48       | 0.04           |

$^a$ $A_V/E_{B-V} = 3.1$; Howarth 1983 and Seaton 1979.

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Therefore, we took the opportunity to write and fully test a new code that models the light from an X-ray–irradiated Roche lobe–filling star and accretion disk orbiting a compact object. The model includes a flared accretion disk, new model atmosphere fluxes, and limb-darkening coefficients for cool stars. Also, we now use a robust genetic-type algorithm (Storn & Price 1995) to fit the light curves. Unlike the algorithm used in Paper I and most other studies, genetic codes have been used before in fitting light curves, as in Metcalfe (1999), Gelino, Harrison, & Orosz (2001), and Orosz et al. (2002): the best-fit solution does not depend on the starting parameters. Hence, we are able to improve on the accuracy of the mass determination for the binary components of XTE J2123–058.

4.1. The X-Ray Binary Model

To interpret the optical light curves, we used a model that includes a Roche lobe–filling secondary star, the effects of X-ray heating on the secondary, a concave accretion disk, shadowing of the secondary star by the disk, and mutual eclipses of the disk and secondary star. For details of the model, see Tjemkes et al. (1986) and Orosz & Bailyn (1997). The geometry of the binary system is given by the orbital inclination $i$, the mass ratio $q = M_2/M_1$ (where $M_1$ and $M_2$ are the masses of the compact object and secondary star, respectively), and the Roche lobe–filling factor $f$ of the secondary star. The light from the secondary star is given by its mean effective temperature ($T_{\text{eff}}$), the gravity darkening exponent $\beta$, and the X-ray albedo $W$. The temperature across the star is scaled such that its weighted mean matches the observed temperature.

The light from the accretion disk is given by its radius $R_{\text{disk}}$, defined as a fraction of the distance to the inner Lagrangian point ($R_{\text{L}}$), its flaring angle, $\alpha$, the temperature at the outer edge of the disk ($T_{\text{out}}$), and the exponent on the power-law radial temperature distribution, $\xi$. Finally, the additional light due to X-ray heating is given by the unabsorbed X-ray flux ($F_{X,0}$), the distance to the source ($d_{\text{gc}}$), and the orbital separation [determined from the optical mass function $f(M)$, $P_{\text{orb}}$, the $q$, and $i$]. The X-ray heating of the secondary star is computed in the same way as described by Tjemkes et al. (1986). We assume that the secondary is in synchronous rotation and completely fills its Roche lobe. Since the late-type secondary star has a convective envelope, we fix the gravity darkening exponent to 0.08 (Lucy 1967). The albedo of the companion star ($W$) is fixed at 0.40 (de Jong, van Paradijs, & Augusteijn 1996). For ease, the key variables are listed in Table 3.

4.1.1. The Accretion Disk

The model assumes a flared, concave accretion disk of the form $h \propto r^{9/7}$ with $h$ and $r$ the disk height and radius, respectively (Vrtilek et al. 1990). The radial distribution of the temperature across the disk is given by $T(r) = T_{\text{out}}r^2$. For a steady-state, optically thick, viscous accretion disk, the exponent of the power law is $-3/4$ (Pringle 1981). For a disk heated by a central source, the exponent is $-3/7$ (Vrtilek et al. 1990). The temperature of the accretion disk’s rim is fixed at $T_{\text{out}}$. We assume that the disk radiates as a blackbody. For a given local temperature in the accretion disk, we calculate the blackbody intensity over the wavelength range of the filter and then convolve it with the response of the filter.

4.1.2. The Intensity Distribution

The intensity distribution on the secondary star is calculated using PHOENIX-model atmospheres colors that are publicly available on the World Wide Web. PHOENIX is a multipurpose state-of-the-art stellar atmosphere code that can calculate atmospheres and spectra of stars all across the Hertzsprung-Russell diagram (Hauschildt, Allard, & Baron 1999). The colors that are available cover a range of temperatures (1700–30,000 K), gravity (log $g = 3.5–5.0$), and wavelength and have been already convolved with standard filter responses. For this code to be of general use, it is important that one can calculate model atmospheres for cool stars.

In order to accurately calculate the intensity at each grid point on the star, which depends on the local temperature and gravity, we use a two-dimensional bicubic spline interpolation method (Press et al. 1992) using the two-dimensional color grid.

We use a quadratic limb-darkening law to correct the intensity from the star and accretion disk. The coefficients are taken from Claret (1998) and were computed using PHOENIX-model atmospheres. These calculations extend the range of effective temperatures 2000–50,000 K and gravity log $g = 3.5–5.0$. Again, we use a two-dimensional bicubic spline interpolation method to calculate the coefficients for a given temperature and gravity.

4.2. The Fitting Algorithm

The minimization of a function is a difficult one, especially if the function is complicated and has many parameters that are correlated and even more so if there are many isolated local minima or more complicated topologies. Methods such as Powell (a maximum-gradient technique) and downhill simplex (polyhedral search technique) are good only if the global minimum lies near the initial guess values: this is not normally the case for complicated functions. When the objective function is nonlinear, direct search methods using algorithms such as Nelder & Mead’s (1965) or genetic algorithms are the best approaches (Press et al. 1992).

The basic strategy at the core of every direct search method is to generate variations of the parameter vectors...
and make a decision whether or not to accept the newly derived parameters. A new parameter vector is accepted if and only if it reduces the value of the objective function. Although this process converges fairly fast, it runs the risk of becoming trapped by a local minimum. Inherently parallel search techniques such as genetic and evolutionary algorithms have some built-in safeguards to ensure convergence. By running several vectors simultaneously, strong parameter configurations can help other vectors escape local minima.

Ideally, an optimization technique should be fast and should find the true global minimum regardless of the initial system parameter values. Storn & Price (1995) have developed a genetic-type technique called “differential evolution” that is robust and simple. Differential evolution generates new parameter vectors by adding the weighted difference vector between two population members to a third member. If the resulting vector yields a lower objective function value than a predetermined population member, the newly generated vector replaces the vector with which it was compared in the next generation. The best parameter vector is also evaluated for every generation in order to keep track of the progress that is made during the minimization process. There are four main parameters in the differential evolution code: NP, the number of population members (usually taken as 10 times the number of fitting parameters); F, the mutation scaling factor that controls the amplification of the difference vector; CR, the crossover probability constant; and itermax, the maximum number of generations. For our problem of minimizing the $\chi^2$ function, we use $CR = 0.9$, $FX = 0.9$, and itermax = 2000, which corresponds to $\sim 100,000$ calculations of the function.

### 4.3. Fitting the Outburst/Decay Data

We use the differential evolution algorithm described in § 4.2 to fit the same phase-binned outburst and decay light curves of XTE J2123–058 that were presented in Paper I. We fix $d_{\text{pc}} = 9.6$, $P_{\text{orb}} = 0.2482$ days, and $T_{\text{eff}} = 4250$ K corresponding to a K7 star (Paper II). The observed X-ray flux (ASM 2–12 keV energy range) during the time of the outburst and decay data sets was $1.7 \times 10^{-9}$ ergs cm$^{-2}$ s$^{-1}$ and $1.7 \times 10^{-10}$ ergs cm$^{-2}$ s$^{-1}$, respectively. The $R$-band reddening is fixed to be 0.27 mag based on $E_{B-V} = 0.12$ (Hynes et al. 2001). The model parameters that we fit are $g$, $i$, $R_{\text{disk}}$, $\alpha$, $T_{\text{out}}$, and $\xi$.

For the outburst light curve with 29 data points, we find a minimum reduced $\chi^2_2$, $\chi^2_2$ of 0.9 at $g = 0.36$, $i = 72.5^\circ$, $R_{\text{disk}} = 0.69 R_{\text{L1}}$, $\alpha = 59^\circ$, $\xi = -1.26$, and $T_{\text{out}} = 2.5 \times 10^4$ K. In order to determine the uncertainty in the parameters of interest, we perform a one-dimensional grid search and plot the 68% and 90% confidence levels (see Table 4 and Fig. 2). If we use a distance of $d_{\text{pc}} = 11$, the minimum $\chi^2$ is not significantly different (at the 90% level). The inclination is the same; however, $\alpha$ increases by $3.5^\circ$. This is because the model needs to increase $\alpha$ in order to shield the secondary star from the strong X-ray heating ($L_X = 2.5 \times 10^{33}$ ergs s$^{-1}$ for $d_{\text{pc}} = 11.0$ compared with $L_X = 1.9 \times 10^{33}$ ergs s$^{-1}$ for $d_{\text{pc}} = 9.6$).

Since the quality of the outburst light curve is much better than the decay light curve, the eclipse features at orbital phases 0.0 and 0.5 are more evident. Hence, the parameters derived from modeling the outburst light curve will be more accurate compared to those derived from the decay light curve. Therefore, for the decay light curve with 20 data points, we fix $i$ and $g$ derived from the outburst light curve and determine $R_{\text{disk}}$ and $\alpha$ of the accretion disk. We find a minimum $\chi^2_2$ of 1.5 at $R_{\text{disk}} = 0.56 R_{\text{L1}}$, $\alpha = 59^\circ$, $\xi = -1.19$, and $T_{\text{out}} = 7505$ K (see Table 4). The best model fits to the outburst and decay light curves are shown in Figures 3 and 4, respectively. We also show the different components of light in the model, i.e., the accretion disk, the rim of the disk, and the X-ray–heated secondary star. It should be noted that changing $T_{\text{eff}}$ does not have a significant effect on the light curves: its effect is significant only at the 0.4% level. This is because of the dominant effect of X-ray heating. Changing the albedo of the companion star to 0.30 and 0.5 (de Jong, van Paradijs, & Augusteijn 1996; Milgrom & Salpeter 1975) gives a worse $\chi^2$, but it is significantly different only at the 95% level. The derived parameters are the same within the uncertainties.

We can compare the results we obtained from fitting the outburst and decay light curves with our new model and fitting procedure with those obtained in Paper I. The outburst values obtained for $i$ and $\alpha$ in Paper I were significantly underestimated (99% confidence level) compared to those we obtain here. Also, the value we obtain for $g$ in Paper I was significantly underestimated (>99% level) compared to the value given here. The results obtained

### Table 4

| Parameter   | Best Fit | 68% Confidence | 90% Confidence |
|-------------|----------|----------------|----------------|
| $q$.......... | 0.36     | +0.01 to -0.01 | +0.16 to -0.02 |
| $i$ (deg).... | 72.5     | +0.7 to -0.7   | +1.0 to -2.3   |
| $R_{\text{disk}}$ (RL1) | 0.69     | +0.01 to -0.02 | +0.03 to -0.03 |
| $\alpha$ (deg) | 5.9      | +0.2 to -0.5   | +0.5 to -0.7   |

### Outburst Data

| Parameter   | Best Fit | 68% Confidence | 90% Confidence |
|-------------|----------|----------------|----------------|
| $R_{\text{disk}}$ (RL1) | 0.56     | +0.03 to -0.03 | +0.05 to -0.05 |
| $\alpha$ (deg) | 5.2      | +0.5 to -0.6   | +0.9 to -0.8   |

### Decay Data

![Fig. 2.—Values of $\chi^2$ obtained for the outburst data by grid-searching the binary inclination (top panel) and mass ratio (bottom panel) while minimizing the other model parameters. Dashed line: Confidence level of 90%.](image-url)
through fitting the decay light curve agree well with those obtained in Paper I. The difference in the results compared to Paper I is due mostly to the errors in the code and also in the fitting method used to find the global minimum solution (see § 4). The most likely reason that the results from the decay light curve are comparable is the relatively large error bars of the decay light curve. This would naturally give larger uncertainties in the derived parameters, so it is not surprising that the results obtained using the model in Paper I and our new model agree.

Vrtilek et al. (1990) showed that the temperature profile of a flared accretion disk totally dominated by irradiation (isothermal) takes the form $T(r) \propto r^{3/7}$ rather than $T(r) \propto r^{-3/4}$ for a steady-state, nonirradiated disk. The value for the temperature exponent we derive is more negative ($\sim -1.2$) than either of these values. For a fixed outer disk temperature (and geometry), a steeper exponent implies a hotter disk. Therefore, in order to match the observed flux using $\xi = -3/7$, the projected area of the disk in the outer parts must be, on the whole, smaller. Note that this can be achieved if the disk's structure is warped: it has been known for some time that X-ray binaries can produce warped accretion disks (Wijers & Pringle 1999; Ogilvie & Dubus 2001). In order to explain the observed reprocessed X-ray flux in LMXBs, the disk in these systems must be either warped or the central X-ray source is not pointlike (Dubus et al. 1999). With this data set, we cannot determine the shape of the accretion disk. However, it should be noted that multicolor observations throughout an outburst may allow one to determine $\xi$ (see Orosz & Bailyn 1997) and, more importantly, provide information on the shape of the accretion disk in an SXT during outburst.

4.4. The Shape of the Light Curves

At the start of an outburst, angular momentum in the disk is transferred to the outer parts, so matter diffuses inward and the disk radius expands. When the system's brightness decays, the disk shrinks in radius. The changes observed in the light curves during decline are primarily caused by large changes in the disk size and geometry. As we can see from the different component fits to the outburst and decay data, in outburst, the irradiated disk light swamps the light from the irradiated secondary star and, hence, the amplitude of the light curve is relatively small. As the irradiation of the disk decreases, the disk temperature is much cooler and the disk radius smaller, so the fraction of light from the disk is small compared to the fraction of light from the secondary star. This results in a large amplitude for the light curve. The triangular-shaped minimum at phase 0.0 in the outburst light curve can be interpreted as the eclipse of the accretion disk by the X-ray–heated secondary star. The deep minimum in the outburst data at phase 0.5, i.e., when the X-ray–heated secondary star is eclipsed by the disk, implies a larger disk radius compared to the disk radius when the X-ray irradiation is less. The same is true for the eclipse features at phase 0.0. The fit to the decay data requires a smaller and cooler, but not significantly thinner, accretion disk compared to the disk in the outburst data. Our model fits imply a change of $\sim 20\%$ in the disk size.

5. THE BINARY MASSES

The masses of the binary components are given by rearranging the equation for the optical mass function,

$$M_1 = \frac{K_2^2 P_{\text{orb}}}{2 \pi G} \frac{(1 + q)^2}{\sin^3 \iota} M_\odot, \quad M_2 = q M_1,$$

where $K_2$ is the radial velocity semi-amplitude and $G$ is the gravitational constant. Substituting our values for $q$ and $i$ with $K_2$ and $P_{\text{orb}}$, we calculate $M_1$ and $M_2$. In order to determine the uncertainties, we use a Monte Carlo simulation in which we draw random values for the observed quantities that follow a given distribution, with mean and variance the same as the observed values. For $K_2$ and $P_{\text{orb}}$, the random
distributions are taken to be Gaussian because the uncertainties are symmetric about the mean value: $K_2 = 287 \pm 12$ km s$^{-1}$, $P_{\text{orb}} = 0.248236 \pm 0.000002$ days (1σ errors; Paper II). However, for $q$ and $i$, the uncertainties are asymmetric and we determine the actual distribution numerically. This is done by first calculating the maximum likelihood distribution using the actual $\chi^2$ fit values (see § 4.2) and then determining the cumulative probability distribution. By picking random values (from a uniform distribution) for the probability, we obtain random values for $q$ and $i$. Figure 5 shows the results of the Monte Carlo with $10^6$ simulations. Table 5 gives the ranges we obtain for the system parameters.

Tomisck et al. (2001) constrain the spectral type of the secondary star to lie in the range K5–K9. We can use the earliest spectral type (K5) for the secondary star to place an upper limit to the mass of the secondary star, since the mass of the secondary must be less than or equal to the main-sequence mass of the same spectral type. A K5 V star has a zero-age main-sequence (ZAMS) mass of 0.68 $M_\odot$ (Gray 1992). Although the present-day mass of the secondary star is lower and the secondary star is metal poor and, hence, will have a lower mass compared to a normal star, we can still use the ZAMS mass as a firm upper limit to the mass of the secondary star. Using this limit, we constrain $M_1$ to lie in the range 1.04–1.56 $M_\odot$ and 0.95–1.68 $M_\odot$ (68% and 90% confidence, respectively), which is consistent with the mass range determined in Paper II and by Tomisck et al. (2001).

**Table 5**

| Parameter | Best Fit | 68% Confidence | 90% Confidence |
|-----------|----------|----------------|----------------|
| $M_1$     | 1.30     | 1.04–1.70      | 0.95–1.92      |
| $M_2$     | 0.46     | 0.36–0.83      | 0.32–0.98      |
| $R_2$     | 0.59     | 0.54–0.74      | 0.53–0.76      |

6. THE QUIESCENT LIGHT CURVE OF XTE J2123–058

In Figure 6, we show our new quiescent optical light curve of XTE J2123–058 obtained at different times, phase-folded using the ephemeris given in Paper II. Overall, the shape and mean brightness level of the light curves are very similar for data taken at three different epochs over a year. This is in contrast to the optical light curve of other SXTs, e.g., Cen X-4 and A0620–00, whose light curves are known to change shape and mean brightness (McClintock & Remillard 1990; Leibowitz, Hemar, & Orio 1998; Gelino, Harrison, & Orosz 2001). Such changes have been attributed to dark spots on the surface of the late-type companion star, which are thought to migrate on timescales of a few months to years (Bouvier & Bertout 1998).

One expects the quiescent light curves of X-ray transients to be dominated by the ellipsoidal variations of the secondary star, which gives rise to a double-humped modulation, where the maxima are equal and the minima are unequal for high-inclination systems. However, the quiescent light curve of XTE J2123–058 is far from being clean: the minimum at phase 0.0 (inferior conjunction of the secondary star) appears to be offset by $\sim$0.04 in phase. In an attempt to try and understand this light curve, we consider the following two cases: (A) where we match the amplitude of the light curve between phase 0.0 and 0.5 and (B) where we match the light curve between phase 0.5 and 1.0 with our X-ray binary model (see Fig. 7).

From the residuals for these two cases, we can see that there is either excess light around phase 0.15 (case A) or a lack of light, i.e., a dip around phase 0.8 (case B). The excess light near phase 0.15 does not coincide with where a bulge is expected, i.e., the region where the gas stream impacts the edge of the accretion disk. Bright spots normally precede the secondary star and are observed around orbital phase $\sim$0.8–0.9 (see Wood et al. 1986, 1989 for examples of the bright spot in high mass ratio quiescent dwarf novae). Given the high binary inclination of XTE J2123–058, one can envisage situations in which the inner part of the accretion disk is eclipsed by a bulge. If the bulge itself does not emit much light compared to the accretion disk, then the net effect on the light curves would be a decrease in light near phase 0.8. Similar effects have been seen in the UV light curves of Z Cha during superoutburst. In Z Cha, the dip at phase 0.8 was explained as being due to vertical disk structure occulting the hot inner disk (Harlaftis et al. 1992). Therefore, in the next section, we assume that the dip near phase 0.8 is due to the bulge eclipsing the inner parts of the accretion disk.

6.1. Fitting the Quiescent Light Curve

The three quiescent $R$-band light curves of XTE J2123–058 were combined and binned into 30 phase bins. The parameters in the X-ray binary model that we vary are $i$, $T_{\text{eff}}$, $F_X$, $R_\text{disk}$, $T_{\text{out}}$, and $\xi$. We fix $d_{\text{pc}} = 9.6$ and the $R$-band reddening to be 0.27 mag. In our initial fits, we let $\alpha$ run as a free parameter, but we found that it did not make a significant difference to the fits. (In fact, an F-test on the best-fit values does not justify the addition of an extra parameter. Therefore, we fixed its value to 2°, i.e., we assume a geometrically thin accretion disk.) Given the determination of the veiling of the $R$-band light, we impose the condition that the accretion disk cannot contribute more than 33% to the observed light (using the upper limit.
of 77% for the secondary star’s contribution to the observed flux; see Paper II). When one determines the veiling of an absorption line spectrum, one compares the strength of the absorption lines of a template star (which normally has solar metallicity) with the target spectrum. If the target has a metal-poor spectrum, then the veiling will be overestimated. Given the high Galactic latitude and systemic velocity of XTE J2123–058, the possibility that it is a halo metal-poor system cannot be ruled out. Hence, we use the veiling estimated in Paper II as a firm upper limit to allow for the possibility that the veiling may be overestimated. We do not attempt to include an accretion disk bulge in the X-ray binary model because the height and temperature of the bulge most probably varies with orbital phase, thus introducing many parameters that would be difficult to deconvolve. Instead, we model the accretion disk light eclipsed by the bulge as a Gaussian function that is included in the fitting algorithm.

We use the differential evolution algorithm (see § 4.2) to fit the phase-binned light curve. For the fits with $q = 0.36$, we find a minimum $\chi^2$ of 1.2 at $i = 71.8^\circ$, $T_{\text{eff}} = 4610$ K, $T_{\text{disk}} = 1425$ K, $R_{\text{disk}} = 0.45 R_{L1}$, $\log F_{X,0} = -12.99$ ergs cm$^{-2}$ s$^{-1}$, and $\xi = -1.23$. The bulge is centered at 0.84 ± 0.01 phase and has a Gaussian width and height of 0.12 ± 0.01 phase and $-0.12 ± 0.01$ mag, respectively. A one-dimensional grid search was performed to determine the uncertainties in the fitted parameters (see Table 6). For the fits with $q = 0.48$, the minimum $\chi^2$ changes by less than 0.2, and the derived parameters are the same. The best model fit to the quiescent light curve and the different components in the model, i.e., the accretion disk, the X-ray–heated secondary star, and the bulge are shown in Figures 8 and 9, respectively. Changing the secondary star’s albedo to 0.3 and 0.5 does not change the $\chi^2$ of the fits significantly: the $\chi^2$ changes by only 0.05. Also, using a gravity darkening exponent of 0.10 does not change the fits: the $\chi^2$ changes by only 0.07. With the exception of $W$, within the uncertainties, the derived parameters are not different. For $W = 0.3$ and 0.5, we obtain $\log F_{X,0} = -13.12$ and $-12.81$ ergs cm$^{-2}$ s$^{-1}$, respectively. Using the distance of 9.6 kpc and the X-ray flux obtained from the fits, we obtain an unabsorbed X-ray luminosity of $1.2 \times 10^{33}$ ergs s$^{-1}$ for XTE J2123–058 in quiescence.
The binary inclination angle we obtain by fitting the quiescent light curve is similar to what was obtained by fitting the outburst data (see § 4.3). The value we obtain for $T_{\text{eff}}$ implies a K5 spectral type, which is consistent (within the uncertainties) with the classification of the secondary star using the absorption lines (see Paper II). To see if our interpretation of the disk bulge eclipse is correct, we added a bulge to the accretion disk rim.

To illustrate its effect, we compute a model light curve that is shown in Figure 10. We fix the system parameters to the best-fit values derived earlier. We varied the height of the bulge and the orbital phase range in which it lies in order to match the observed light curve. The bulge was chosen to have a constant arbitrary height of 17$^\circ$ (i.e., the flare angle at the edge of the disk) and constrained to lie between orbital phase 0.65 and 1.0. The temperature of the bulge is taken to be the same as the temperature of the disk’s edge. As one can see, the model clearly predicts less flux near phase 0.8, which is due to the eclipse of the X-ray–heated disk by the cooler disk bulge.

7. DISCUSSION

7.1. The Accretion Disk Radius

We have measurements of the accretion disk radius in XTE J2123–058 at three different stages of its outburst: near the peak of outburst, during decay, and in quiescence (Table 7). The accretion disk radius we measure for XTE J2123–058 in quiescence is consistent with that measured in other SXTs. Although theoretically we cannot comment exactly on how the disk size changes with time, it should be noted that it is plausible that the disk radius decays exponentially as is inferred in dwarf novae (Smak 1984).

7.2. The Mass of the Neutron Star

Observationally, the mean mass of neutron stars in binary radio pulsars is $1.38 \pm 0.07\ M_\odot$ (Thorsett & Chakrabarty 1999). The model of Fryer & Kalogera (2001) agrees well with this observed peak. They determined the neutron star and black hole initial mass function and find that 81%–96% of neutron stars lie in the mass range between 1.2 and $1.6\ M_\odot$. Within this framework, the current mass of the neutron star in XTE J2123–058 (1.30 $M_\odot$; Table 5) may be the mass at its formation. However, in LMXBs, one expects massive neutron stars to exist because the neutron star has been accreting at the Eddington rate for a long period of time (Zhang, Strohmeyer, & Swank 1997). The observations of kilohertz quasi-periodic oscillations in some neutron star LMXBs suggests that neutron stars could be as massive as $2\ M_\odot$. If the neutron stars in LMXBs are formed with a mass of $1.4\ M_\odot$, then it is quite possible to accrete an extra $0.6\ M_\odot$ in $10^8\ yr$ (Zhang et al. 1997).

7.3. The Secondary Star and Outburst Mechanism

The transient behavior in LMXBs has been discussed by King et al. (1996) and van Paradijs (1996). In the model of King et al. (1996), for a given magnetic braking law, the

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**Fig. 8.**—Observed quiescent R-band light curve of XTE J2123–058 (crosses) and the best model fit (solid line). Dashed lines: Model with no X-ray heating. For clarity, 1.5 orbital cycles are shown.

**Fig. 9.**—Separate components in the X-ray binary model that give the best fit to the quiescent data. The accretion disk and bulge are shown along with the X-ray–heated secondary star and the total observed flux. For clarity, 1.5 orbital cycles and dereddened fluxes are shown.
mass transfer rate is smaller in black hole X-ray binaries than in neutron star X-ray binaries. Short-period neutron star X-ray binaries will be transient only if their companions are highly evolved, because the mass transfer rates in binaries with evolved companions are smaller than in systems with unevolved companions. A system will be transient if the average mass transfer rate \(-M_2\) is smaller than some critical value \((-M_2)_{\text{crit}}\). Although we find \(-M_2/M_{\text{crit}}\) to be at least a factor of 4 obtained using our 90\% mass limits for the binary components and the equations for \(-M_2\) and \(M_{\text{crit}}\) given in King et al. (1996), there are many uncertainties in how the mass transfer rates are determined (see Paper II). The magnetic braking mechanism is not very well understood (Kalogera, Kolb, & King 1998), and it could be that the mass transfer rate we see is not the secular mean. Also, XTE J2123–058 may have had a very different evolutionary path compared to other SXTs. The system may be a remnant of a thermal-timescale mass transfer, leading to peculiarities close to the end of the thermal phase (A. R. King 2002, private communication).

7.4. The X-Ray–heated Secondary Star

The H\(\alpha\) Doppler map of XTE J2123–058 in quiescence presented in Paper II shows significant emission arising near the inner Lagrangian point, which could be due to the X-ray heating or chromospheric activity on the secondary star. Our fits require the inner face of the secondary star to be heated in order to match the observed shape of the minimum at phase 0.5. The dashed line in Figure 8 shows a model light curve with no X-ray heating. It has been known for some time that strong X-ray heating in an interacting binary can affect the form of the light curve (van Paradijs & McClintock 1995). X-ray heating changes the photometric light curve by adding light to the minimum at phase 0.5 and changes the radial velocity curve by shifting the effective center of the secondary, weighted by the strength of the absorption lines, from the center of mass of the star, resulting in a significant distortion of the radial velocity curve.

The X-ray heating is such that the inner face of the secondary star is hotter than the outer face. We can estimate the expected change in temperature between the inner and outer faces of the secondary star. Using the X-ray binary model, we computed the orbital variation in the \((V-R)\) color of the secondary star with and without X-ray heating. We find the color difference between orbital phase 0.0 and 0.5 to be very small, 0.02 mag, which corresponds to a temperature change of only \(~60\) K. Such a small temperature change would be very difficult to detect.

In order to investigate the effects of X-ray heating, we computed the radial velocity of the secondary star using a crude treatment for X-ray heating (Phillips, Shahbaz, & Podsiadlowski 1999), where we impose the condition that if the incident flux from the X-ray source is more than 50\% of the intrinsic flux from the secondary star, then the absorption line flux is set to zero. Given the X-ray luminosity, we estimate that such a level of irradiation will distort the radial velocity curve of the secondary star by \(~3\%\). However, given the faintness and, hence, the accuracy of the radial velocity curve, this effect would not be currently measurable.

The late-type companion stars in X-ray transients are perfect candidates to show chromospheric activity. This is because these stars are tidally locked in short orbital periods and, hence, have rapid rotation rates. The chromospheric activity would be present in the form of narrow H\(\alpha\) and Ca ii emission. Although Casares et al. (2002) detect H\(\alpha\) emission at the inner Lagrangian point, it is difficult to say if this emission is solely due to chromospheric activity since the H\(\alpha\) emission can also be powered by X-ray heating. However, we can ask how much of the H\(\alpha\) emission can, in principle, be powered by X-ray heating. To do this, we need to compare this predicted emission rate from the X-ray source with the observed H\(\alpha\) photon emission rate.

The rate of emission of photons \(N_p\) with a given energy is given by

\[
N_p = \frac{F_p \lambda d^2}{E_p},
\]

where \(F_p\) is the photon flux, \(d\) is the distance to the source, and \(E_p\) is the energy of the photon. From the H\(\alpha\) Doppler map (Paper II), we estimate the fractional contribution of the emission on the secondary star relative to the total H\(\alpha\) emission. We then use this fraction with the equivalent width of the whole H\(\alpha\) emission line to estimate the width of the narrow component, which we find to be \(~1\) Å. This combined with the dedereeden R-band magnitude (\(m_R = 21.8, E_{R-V} = 0.12\); Hynes et al. 2001) thus gives an H\(\alpha\) photon flux of \(1.7 \times 10^{-18}\) ergs cm\(^{-2}\) s\(^{-1}\), which

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**TABLE 7**

| \(\Delta t^*\) (days) | \(R_{\text{disk}}\) \((R_{\odot})\) | log \(F_X\) (ergs cm\(^{-2}\) s\(^{-1}\)) |
|----------------------|----------------|------------------|
| 29........| 0.69 ± 0.02 | −7.77  |
| 48........| 0.56 ± 0.03 | −8.77  |
| 551......| 0.45 ± 0.21 | −12.99 |
corresponds to an emission rate of $N_{\text{H}_\alpha} = 4.1 \times 10^{40}$ photons s$^{-1}$ ($d_{\text{kpc}} = 9.6$ and $E_{\text{H}_\alpha} = 1.9$ eV).

In order to calculate the X-ray photon flux, we assume that each X-ray photon causes one photoionization of H $\text{I}$ and a fraction $\eta$ then recombine to produce an H$\alpha$ photon. The fraction is given by the ratio of the recombination rate of H$\alpha$ to the total recombination rate of H $\text{I}$ as a whole and is taken to be 0.45 for case B recombination (Hummer & Storey 1987). One also has to allow for the fact that only a fraction of the high-energy photons actually cause photoionization. This fraction, $f_\text{ph}$, depends on the solid angle subtended by the secondary star and the accretion disk at the compact object, which is $\Omega_{\text{star}} = \pi (R_d/a)^2 (= 0.28)$ for the star, whereas the planar disk that shields the secondary star subtends a solid angle of $\Omega_{\text{disk}} = 4(R_d/a)\tan \alpha (= 0.04$; where $R_d$ is the accretion disk and $a$ is the binary separation). Using these values we estimate $f_\text{ph} = 0.24$. Finally, one needs to allow for the X-ray albedo of the secondary star, which is taken to be 0.4 (de Jong, van Paradijs, & Augusteijn 1996). Assuming that the inferred unabsorbed X-ray flux (see § 6.1) has a mean energy of 2 keV, a distance of 9.6 kpc, and allowing for factors mentioned above, we obtain the X-ray photon flux of $N_{\text{X-ray}} = 1.0 \times 10^{41}$ photons s$^{-1}$. Since the predicted number of X-ray photons that produce H$\alpha$ photons is larger than the actual number observed, we conclude that the H$\alpha$ observed from/near the secondary star can, in principle, be powered by X-ray heating.

7.5. Comparison with Other Neutron Star SXTs

The X-ray luminosity in quiescence we derived for XTE J2123$-$058 is comparable with that observed in other neutron star SXTs, typically $10^{32}$–$10^{33}$ ergs s$^{-1}$. Although there is some debate as to the origin of these quiescent X-rays, accretion seems to be the dominant source. Brown, Bildsten, & Rutledge (1998) suggest that the X-rays could be due to the cooling of the neutron star's crust, which is heated during outburst. However, as pointed out by Narayan, Garcia, & McClintock (2001), neutron star SXTs have about half their total luminosity in their X-ray power-law tails, which is most likely to be produced by accretion rather than crustal cooling. Also, recent Chandra X-ray observations of Aql X-1 in quiescence show that the X-ray luminosity varies on timescales that are not consistent with the heated neutron star crust model (Rutledge et al. 2001). It should be noted that the observed X-ray flux in XTE J2123$-$058 is also too high to be due to the coronal emission from the companion. Following Bildsten & Rutledge (2000), we estimate the X-ray/bolometric flux ratio $F_{\text{X}}/F_{\text{bol}}$ to be 3.7, i.e., similar to what is observed in other quiescent neutron star SXTs.

Normally, the X-ray luminosities of SXTs are obtained by direct X-ray observations of the source. Our optical study of XTE J2123$-$058 in quiescence has allowed us to infer the quiescent X-ray luminosity. What would be of great interest is a direct confirmation of the X-ray flux through direct measurements.

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