Interference of stimulated electronic Raman scattering and linear absorption in coherent control

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(Dated: June 26, 2014)

We consider quantum interference effects in carrier and photocurrent excitation in graphene using coherent electromagnetic field components at frequencies ω and 2ω. The response of the material at the fundamental frequency ω is presented, and it is shown that one-photon absorption at ω interferes with stimulated electronic Raman scattering (combined 2ω absorption and ω emission) to result in a net contribution to the current injection. This interference occurs with a net energy absorption of ħω and exists in addition to the previously studied interference occurring with a net energy absorption of 2ħω under the same irradiation conditions. Due to the absence of a bandgap and the possibility to block photon absorption by tuning the Fermi level, graphene is the perfect material to study this contribution. We calculate the polarization dependence of this all-optical effect for intrinsic graphene and show that the combined response of the material at both ω and 2ω leads to an anisotropic photocurrent injection, whereas the magnitude of the injection current in doped graphene, when transitions at ω are Pauli blocked, is isotropic. By considering the contribution to coherent current control from stimulated electronic Raman scattering, we find that graphene offers tunable, polarization sensitive applications. Coherent control due to the interference of stimulated electronic Raman scattering and linear absorption is relevant not only for graphene but also for narrow-gap semiconductors, topological insulators, and metals.

PACS numbers: 73.50.Pz, 42.65.Dr, 78.67.Wj, 42.65.-k

I. INTRODUCTION

Coherent control (CC) involves the interference between multiple excitation pathways to acquire a handle on the final state of a quantum-mechanical process.1 Applied to semiconductor optics, the typical CC experiment uses light at a fundamental frequency ω and its second harmonic 2ω. Interference between the transition amplitudes for two-photon absorption (2PA) at ω and one-photon absorption (1PA) at 2ω results in an unbalanced distribution of carriers in momentum space, providing a net photocurrent.2–5 The two-color electromagnetic field provides the energy necessary to create electron-hole pairs in the sample, and the injected charge carriers acquire their velocities according to the band dispersion.6

In the typical operation regime for conventional semiconductors such as GaAs, ħω would lie within the bandgap; the light frequencies in such experiments are regularly selected according to ħω < Eg < 2ħω, where Eg is the bandgap energy, so that 1PA at ω is energetically forbidden, and the lowest energetically-allowed perturbative order for absorption of the fundamental is the second order. However, for ħω > Eg, the fundamental is absorbed at first order, and how this affects the CC is especially important to understand for narrow-gap semiconductors. Gapless materials such as graphene further present the possibility of studying CC in interesting ways by substituting the bandgap Eg with 2|μ|, where μ is the chemical potential. The range of applicability of previous theories can thus be handily tested by varying the doping level or an applied gate voltage, and scenarios lying outside the typical operation regime are readily accessible. In particular, for ħω > 2|μ|, linear absorption of the fundamental beam occurs, which has not been carefully considered in early studies of coherent optical injection and control in carbon nanotubes,7–9 graphene,10–13 and other semiconducting materials.1–6

In the presence of coherent ω and 2ω fields, linear absorption at ω is not the only process with a net energy absorption of ħω; at the next perturbative order the combined absorption of a 2ω photon and the emission of a ω photon must also be considered. This nondegenerate two-photon transition process is an instance of stimulated electronic Raman scattering (ERS),14–16 where light is scattered inelastically and energy is deposited into the electronic state of the system, and was recently studied in the nonlinear optical response of graphene17 and topological insulators.18 Since ERS at ω has the same initial and final state as 1PA at ω, quantum interference occurs between these two transition pathways. Moreover, since the typical CC term between 1PA and 2PA occurs at 2ω rather than ω, there are in effect two distinct interference channels.

In this paper, we consider the carrier response to a two-color field due to the ERS transition amplitude, first generally by presenting a microscopic expression derived from Fermi’s golden rule, then specifically for the case of graphene. For linearly-polarized light, it is shown that current injection in graphene becomes anisotropic with respect to the angle between the linear polarization axes of the light when the new contribution is considered, and that this polarization sensitivity can be tuned by adjusting the chemical potential of the sample. The current injection resulting from the quantum interference between 1PA and ERS is five times stronger with perpendicular polarization axes compared to parallel polarization axes of the light. In contrast, the typical interference term between 1PA and 2PA in graphene results in a current magnitude independent of the polarization of the light.11 The polarization sensitivity is adjustable, via the chemical potential, between a completely isotropic current, to a strongly anisotropic current response where the two contributions to current injection are balanced to exactly cancel each other under perpendicular orientation of the polarization axes.
We derive the microscopic form of the response tensors for carrier and photocurrent injection via quantum interference of 1PA and ERS in Sec. II. We consider the case of graphene, explicitly calculate the response tensors, and present a complete picture of two-color coherent current control via quantum interference of one- and two-photon processes in this material in Sec. III. Finally, we conclude in Sec. IV.

II. TWO-COLOR INTERFERENCE AT $\hbar \omega$

In the presence of a two-color optical field with frequency components $\omega$ and $2\omega$, the conventional injection current as originally described by Atanasov et al.\textsuperscript{3} stems from the cross-term of the following transition amplitudes connecting the same initial and final states: $\Omega^{(1)}_{cv}(2\omega; \bmath{k})$, resulting from light at $2\omega$ to first order in perturbation, and $\Omega^{(2)}_{cv}(\omega; \bmath{k})$, resulting from light at $\omega$ to second order in perturbation. Here $\Omega^{(l)}_{cv}(\omega; \bmath{k})$ is the degenerate $l$-photon transition amplitude between valence band $v$ and conduction band $c$ at wavevector $\bmath{k}$\textsuperscript{19}. The one- and two-photon absorption processes are illustrated by their Feynman diagrams in Fig. 1(a).

The injection term for the current density that results from the coherent interference between the 1PA and 2PA transition amplitudes has the form

$$J^a = \eta^a_{abcd}(\omega)E^{b\nu}(\omega)E^{c\alpha}(\omega)E^{d}(2\omega) + \text{c.c.,} \quad \text{ (1)}$$

where $\eta^a_{abcd}(\omega)$ is a fourth-rank tensor describing the current response of the material, $E^{a\nu}(\omega)$ is the electric field component at frequency $\omega$ ($2\omega$), and repeated indices are summed over Cartesian directions. The tensor is given explicitly for a two-dimensional material by:

$$\eta^a_{abcd}(\omega) = \frac{\pi e^4}{\hbar^2 \omega} \sum_{c', v'} \int \frac{d^2 k}{2\pi^2} [v^a_{cv}(\bmath{k}) - v^a_{cv'}(\bmath{k})]$$

$$\times w^{abc}_{cv}(\bmath{k}) \delta (\omega_{cv}(\bmath{k}) - 2\omega) \quad \text{ (2)}$$

where $e = |e|$ is the electron charge,

$$w^{abc}_{cv}(\bmath{k}) = \sum_{m} \frac{v^b_{cm}(\bmath{k})v^c_{mv}(\bmath{k}) + v^c_{cm}(\bmath{k})v^b_{mv}(\bmath{k})}{\omega_{cm}(\bmath{k}) + \omega_{mv}(\bmath{k})}, \quad \text{ (3)}$$

and leads to the well-known linear absorption of $\omega$ light. The first and second diagrams of Fig. 1(b) show the nondegenerate two-photon process; a $2\omega$ photon is absorbed, a virtual electron-hole pair is created with energy $2\hbar\omega$, and a $\omega$ photon is emitted by either the electron (second diagram) or the hole (third diagram), reducing the energy of the electron-hole pair to $\hbar\omega$. This is an instance of a stimulated electronic Stokes-Raman process\textsuperscript{14–16} known to induce a two-color optical Kerr effect.\textsuperscript{20–23} We calculate the $\bmath{k}$-dependent transition amplitude in the single-particle approximation at the level of Fermi’s golden rule, and find

$$\Omega^{(1)}_{cv}(\omega; \bmath{k}) = \frac{i e^2}{\hbar \omega} v^a_{cv}(\bmath{k}) E^{a\nu}(\omega) \quad \text{ (4)}$$

and the second and third diagrams of Fig. 1(b) show the nondegenerate two-photon process; a $2\omega$ photon is absorbed, a virtual electron-hole pair is created with energy $2\hbar\omega$, and a $\omega$ photon is emitted by either the electron (second diagram) or the hole (third diagram), reducing the energy of the electron-hole pair to $\hbar\omega$. This is an instance of a stimulated electronic Stokes-Raman process\textsuperscript{14–16} known to induce a two-color optical Kerr effect.\textsuperscript{20–23} We calculate the $\bmath{k}$-dependent transition amplitude in the single-particle approximation at the level of Fermi’s golden rule, and find

$$\Omega^{(2)}_{cv}(2\omega, -\omega; \bmath{k}) = \frac{e^2}{\hbar^2 \omega^2} w^{ab}_{cv}(\bmath{k}) E^{a\nu}(\omega) E^{b}(2\omega), \quad \text{ (5)}$$

where

$$w^{ab}_{cv}(\bmath{k}) = \sum_{m} \left( \frac{v^a_{cm}(\bmath{k})v^b_{mv}(\bmath{k})}{\omega_{cm}(\bmath{k}) + \omega_{mv}(\bmath{k})} + \frac{v^b_{cm}(\bmath{k})v^a_{mv}(\bmath{k})}{\omega_{cm}(\bmath{k}) - \omega_{mv}(\bmath{k})} \right). \quad \text{ (6)}$$

The first term within the summation in Eq. (6) corresponds to the second diagram of Fig. 1(b), the latter term corresponds to the third diagram.
The injection rate for the expectation value of any operator $\Theta$ is then calculated up to second perturbative order from $\langle \hat{\Theta} \rangle = i\hbar^{-1} \langle [H, \hat{\Theta}] \rangle$ using matrix elements of the Hamiltonian given by $H_{mn}(k) = \hbar \omega_m(k) \delta_{mn} - \frac{\epsilon}{c} v_{mn}(k) \cdot A(t)$, where $A(t)$ is the vector potential, to obtain

$$\langle \hat{\Theta} \rangle = 2\pi \sum_{c,v} \int \frac{d^3k}{4\pi^2} \langle c,v,k | \Theta | c,v,k \rangle$$

$$\times \left( \left| \Omega^{(1)}_{cv}(\omega,k) + \Omega^{(2)}_{cv}(2\omega,-\omega,k) \right|^2 \delta(\omega_v(k) - \omega) + \left| \Omega^{(1)}_{cv}(2\omega,k) + \Omega^{(2)}_{cv}(\omega,k) \right|^2 \delta(\omega_v(k) - 2\omega) \right). \quad (7)$$

The two summands within brackets describe electron-hole pairs of energy $\hbar \omega$ and $2\hbar \omega$, respectively. The latter yields the typical CC term described by Eq. (2) that has been the subject of previous studies; we thus focus on the former. Taking the occupation number operator as $\Theta$ yields the injection rate for electron-hole pair creation at $\hbar \omega$,

$$\hat{n}(\omega) = \hat{\xi}^{ab}_{c}(\omega) E^{a}c(\omega) E^{b}c(\omega)$$

$$+ \left[ \hat{\xi}^{abcd}_{cv}(\omega) E^{a}c(\omega) E^{bs}c(2\omega)c + c.c. \right]$$

$$+ \hat{\xi}^{abcd}_{cv}(2\omega,c) E^{a}c(2\omega)c E^{bs}c(\omega) E^{d}c(\omega). \quad (8)$$

The first term is one-photon carrier injection due to 1PA, the third term is nondegenerate, two-photon carrier injection (at $\omega$) due to ERS, and the second term is their interference. The quantities $\hat{\xi}_1$, $\hat{\xi}_2$ and $\hat{\xi}_2$ are second-, third- and fourth-rank tensors describing the material part of the response. The 1PA carrier injection tensor is described elsewhere.$^1$ The response tensor describing the interference is given by

$$\hat{\xi}^{abcd}_{cv}(\omega) = \frac{2\pi e^4}{\hbar^3 \omega^3} \sum_{c,v} \int \frac{d^2k}{4\pi^2} \psi^{d*}_{cv}(k) w^{bc}_{cv}(k) \delta[\omega_v(k) - \omega], \quad (9)$$

and the ERS carrier injection tensor is given by

$$\hat{\xi}^{abcd}_{cv}(2\omega,-\omega) = \frac{2\pi e^4}{\hbar^3 \omega^3} \sum_{c,v} \int \frac{d^2k}{4\pi^2} \psi^{d*}_{cv}(k) w^{bc}_{cv}(k)$$

$$\times \delta[\omega_v(k) - \omega]. \quad (10)$$

The interference term is analogous to coherent population control of electron-hole pairs with net energy absorption of $2\hbar \omega$ in the conventional CC regime and is nonzero for non-centrosymmetric materials.$^24$

Finally, taking the current operator as $\Theta$, the response tensor describing the current injection resulting from interference between ERS and 1PA at $\omega$ is found to be

$$\hat{\eta}^{abcd}_{cv}(\omega) = \frac{\pi e^4}{\hbar^3 \omega^3} \sum_{c,v} \int \frac{d^2k}{4\pi^2} \left[ \psi^{a*}_{cv}(k) - \psi^{a}_{cv}(k) \right]$$

$$\times \left[ \psi^{b*}_{cv}(k) w^{cd}_{cv}(k) + \psi^{e*}_{cv}(k) w^{bd}_{cv}(k) \right] \delta[\omega_v(k) - \omega]. \quad (11)$$

For a three-dimensional material, the integration over reciprocal space in Eqs. (2), (7), (9), (10) and (11) should read $\int d^3k/8\pi^3$.

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**III. ANISOTROPIC PHOTOINDUCED CURRENT INJECTION IN GRAPHENE**

We consider graphene to illustrate the two-color interference effect at $\hbar \omega$ in experimentally accessible conditions. The part of reciprocal space relevant for optical response are the two valleys near K and K’ at the vertices of the hexagonal Brillouin zone, where the electrons follow Dirac-like spectrum [Fig. 2]. The gapless band dispersion has the advantage that a bandgap energy is not a limiting factor for the occurrence of absorption at $\hbar \omega$. Instead, the chemical potential $\mu$ plays the role of the limiting factor. Photocurrent generation via CC includes the contribution from both interference channels presented in the previous section and illustrated in Fig. 2 for graphene. Experimentally, electrically tuning the chemical potential allows one to enter and exit the regime where absorption at $\hbar \omega$ occurs. It is thus possible to identify the ERS contribution.

The diagonalized model Hamiltonian and corresponding velocity operator near the K point of graphene take the form$^{11}$

$$H_0 \rightarrow \hbar v_F \begin{pmatrix} k & 0 \\ 0 & -k \end{pmatrix}, \quad v \rightarrow v_F \begin{pmatrix} \hat{k} & i\hat{\phi} \\ -i\hat{\phi} & -\hat{k} \end{pmatrix}, \quad (12)$$

where $v_F$ is the Fermi velocity, $\mathbf{k} = \hat{k}\hat{z}$ is the in-plane crystal momentum relative to the Dirac point, and $\hat{\phi} = \hat{z} \times \hat{k}$ is an in-plane unit vector perpendicular to $\mathbf{k}$. The treatment for the K’ valley is analogous and its presentation neglected for the remainder of the paper as it simply introduces a degeneracy factor of two, in addition to the spin degeneracy factor of two.

The generation of a photocurrent via CC is best illustrated by the unbalanced carrier distributions in reciprocal space due to the interference effect being constructive or destructive.
be equally allowed, e.g. for intrinsic graphene. The distribution due to conventional CC is
\[
\hat{n}(2\omega; \mathbf{k}) = \left| \Omega_{\text{conv}}^{(1)}(2\omega; \mathbf{k}) + \Omega_{\text{conv}}^{(2)}(\omega; \mathbf{k}) \right|^2 \tag{13}
\]
and occurs on the (outer) circle of radius \( k = \omega / v_F \); the distribution due to ERS-induced CC is
\[
\hat{n}(\omega; \mathbf{k}) = \left| \Omega_{\text{ERS}}^{(1)}(\omega; \mathbf{k}) + \Omega_{\text{ERS}}^{(2)}(2\omega, -\omega; \mathbf{k}) \right|^2 \tag{14}
\]
and occurs on the (inner) circle of radius \( k = \omega / 2v_F \).

For circular polarization [Fig. 3(a,b)] the distributions depend on the angle \( \phi_k = \tan^{-1}(k_x / k_y) \) and the CC parameter \( \Delta \varphi \equiv 2\varphi_k - \varphi_{2\omega} \) relating the phases of the two frequency components. For opposite-circularly polarized \( \omega \) and \( 2\omega \) beams, \( \hat{e}_{2\omega} = -\hat{e}_{\omega} = \sigma^z \), the distributions for the carrier injection with net energy absorption of \( 2\hbar \omega \) and \( \hbar \omega \) vary as \( \hat{n}(2\omega; \mathbf{k}) \propto 1 - \sin(\Delta \varphi + 3\phi_k) \) and \( \hat{n}(\omega; \mathbf{k}) \propto \frac{1}{2} (1 + \sin(\Delta \varphi + 3\phi_k)) \), respectively, neither of which yield a current. For co-circularly polarized beams, \( \hat{e}_{2\omega} = \hat{e}_{\omega} = \sigma^z \), the distributions of \( \hat{n}(2\omega; \mathbf{k}) \propto 1 + \sin(\Delta \varphi - \phi_k) \) and \( \hat{n}(\omega; \mathbf{k}) \propto \frac{1}{2} (1 - \sin(\Delta \varphi \pm \phi_k)) \) yield opposite current contributions, although a net current injection remains. The distributions are plotted for \( \Delta \varphi = \pi / 2 \).

For linearly-polarized beams [Fig. 3(c-f)], without loss of generality the polarization axis \( \hat{e}_{2\omega} \) is chosen along \( \hat{x} \) and the \( k \)-dependent carrier distributions follow
\[
\hat{n}(2\omega; \mathbf{k}) \propto \left| \sin(\phi_k) + i e^{-i \Delta \varphi} \sin(2\phi_k - 2\theta) \right|^2, \tag{15}
\]
\[
\hat{n}(\omega; \mathbf{k}) \propto \left| \sin(\phi_k - \theta) - \frac{1}{2} e^{-i \Delta \varphi} [\sin(2\phi_k - \theta) + 3 \sin(\theta)] \right|^2, \tag{16}
\]
where \( \theta \) is the angle between the polarization axes \( \hat{e}_\omega \) and \( \hat{e}_{2\omega} \). The first term in each of Eqs. (15) and (16) is due to 1PA, the second term is due to 2PA [Eq. (15)] or stimulated ERS [Eq. (16)]. The distributions are shown for \( \Delta \varphi = \pi / 2 \) and the polarization axis \( \hat{e}_{2\omega} \) forming angles of \( \theta = 0 \), 45°, 90°, and 135° with respect to \( \hat{e}_{2\omega} \). For parallel and perpendicular polarization, the current due to the ERS contribution opposes the current due to the conventional injection process; in the latter case, the ERS contribution is strong enough to cause the direction of the net current to flip. For 45° and 135°, the ERS contribution adds a current component along the \( \hat{e}_{2\omega} \) direction, while its component along \( \hat{e}_{2\omega} \) opposes the conventional injection process, although not sufficiently to flip the net current along this direction. The magnitude of the photocurrent is anisotropic in \( \theta \) due to the ERS contribution.

The symmetry of graphene yields \( \eta_{\text{conv}}^{xxx}, \eta_{\text{conv}}^{yyyy} \), and \( \eta_{\text{ERS}}^{yyyy} = \eta_{\text{ERS}}^{yyyy} \) as independent components of the current injection tensor; in addition, the relation 2\( \eta_{\text{ERS}}^{yyyy} = \eta_{\text{ERS}}^{xxx} - \eta_{\text{ERS}}^{yyyy} \) holds since an isotropic band model is considered. The disparity parameter \( d = \eta_{\text{ERS}}^{yyyy} / \eta_{\text{ERS}}^{xxx} \) characterizes the sensitivity of the current injection to the angle \( \theta \) between polarization axes for linearly-polarized \( \omega \) and \( 2\omega \) beams; different values of \( d \) and \( \theta \) lead to injected currents with different magnitude and direction.\(^\text{(11)}\)

The additional current injection term presented in this paper...
yields the following implications for graphene. In the conventional regime [Eq. (2)], the nonzero current injection tensor components were given by

\[ \eta^{xxx}_i = \eta^{xxy}_i = \eta^{xyy}_i = -\eta^{yyx}_i = i\bar{\eta}_i(\omega), \]  

(17)

where

\[ \bar{\eta}_i(\omega) \equiv g_s g_v e^4 v_F^2 (2\hbar \omega)^{-3}, \]  

(18)

with \( g_s = g_v = 2 \) describing spin and valley degeneracy, respectively.\(^{11}\) As a result of this contribution, a current component is injected with effective parameter \( d_{\text{eff}} = -1 \) and the magnitude of this current is \( \theta \)-independent. The ERS contribution, in contrast, is strongly \( \theta \)-dependent: taken on its own it contributes an effective parameter \( d_{\text{eff}} = -5 \), meaning that it yields a current whose magnitude is five times stronger when the beam polarization axes are perpendicular (\( \theta = \pi/2 \)) compared to them being parallel (\( \theta = 0 \)). The nonzero tensor components for this contribution [Eq. (11)] are given by

\[ \eta^{xxx}_i = \frac{1}{3}\eta^{xxy}_i = \frac{1}{3}\eta^{xyy}_i = -\frac{1}{5}\eta^{yyx}_i = -\frac{1}{4}i\bar{\eta}_i(\omega), \]  

(19)

This contribution doesn’t occur if the transition at \( \omega \) is blocked due to the lower level being depleted or the upper level occupied. For intrinsic graphene the two discussed interference channels are equally allowed, the resulting current injection tensor includes both contributions, its components are given by

\[ \eta^{xxx}_i = 3\eta^{xxy}_i = 3\eta^{xyy}_i = 3\eta^{yyx}_i = \frac{3}{4}i\bar{\eta}_i(\omega), \]  

(20)

and the corresponding parallel-perpendicular polarization disparity parameter is \( d = 1/3 \). This value is closer to a typical semiconductor such as GaAs, which has \( |d| \approx 0.2 \) for a fundamental photon energy of about 1 eV (below the onset of 1PA at \( \omega \)).\(^{28}\) For intrinsic graphene the parameter \( d \) is independent of the light frequency, as it would be were the ERS contribution not included.\(^{11}\)

Let us now consider the effect of a finite temperature and nonzero chemical potential on the current injection. The deviation from the semiconductor vacuum state results in the Pauli blocking of optical transitions, as observed in linear absorption.\(^{29}\) Since the two contributions to current injection, Eq. (2) and Eq. (11), occur at different excitation energies, it is possible to partly block the lower-energy transition while retaining the higher-energy one. This allows one to tune the polarization sensitivity of the resulting current. For a \( p \)-doped sample, if \( f_\omega \) is the population of electrons as a function of the energy level \( h\omega \) relative to the Dirac point, then the disparity parameter is

\[ d = \frac{4f_{-\omega} - 5f_{-\omega/2}}{4f_{-\omega} - f_{-\omega/2}}. \]  

(21)

This expression is plotted in Fig. 4, and shows that the allowed values are in the range \(-1 \leq d \leq 1/3 \). Taking \( f_{-\omega/2} = 0 \) yields \( d = -1 \) and corresponds to the previous result with complete blocking of the linear absorption of the fundamental due to the lower level being depleted.\(^{11}\) while the ratio of \( f_{-\omega/2}/f_{-\omega} = 1 \) yields \( d = 1/3 \) and corresponds to the situation presented in Fig. 3. For \( d > 0 \), the injected current in the cross-polarized configuration flips direction due to the ERS contribution. A value of \( d = 0 \) (thick contour line in Fig. 4) corresponds to the complete suppression of the current injection for perpendicular polarization axes; this is achieved by adjusting the population to the ratio of \( f_{-\omega/2}/f_{-\omega} = 0.8 \). Thus, a range of polarization-sensitive and polarization-insensitive configurations are available.

The variation of the current injection characteristics according to temperature and nonzero chemical potential affects our understanding of previous experiments in multilayer epitaxial graphene,\(^{10,12,13}\) as the contribution from a single layer de-
pends on its doping level. The doping level in multilayer epitaxial graphene decreases exponentially from 365 meV for the layer closest to the substrate to zero doping for the top layers, with a charge screening length of one layer. The total current injection across all layers is made up of an isotropic contribution from the few heavily-doped layers near the substrate \((d = -1)\) and an anisotropic contribution from the remaining mostly undoped layers \((d = 1/3)\). In the original experiment the incoming beams were cross-linearly polarized;\(^5\) taking the ERS contribution into account yields counter-propagating currents in the heavily-doped and undoped layers, as illustrated in Fig. 3(e). A subsequent experiment resolved the angular dependence on the polarization axes and found that it did not correspond to the simple model of a single graphene layer.\(^6\) In both experiments the current injection was detected via the emitted THz radiation with the signal collected behind the sample. Light attenuation is stronger for the THz signal than for the frequencies of the incoming beams. Thus, although there are only a few heavily-doped layers, they could contribute relatively strongly to the detected THz signal due to their proximity with the detector. It is realistic to expect the signal to have a value of \(d\) in the range 0.14 to 0.24; the resulting polarization dependence is shown in Fig. 5, and is in good agreement with the polarization-resolved experimental data.\(^7\) Thus the inclusion of the Raman term identified here could lead to an understanding of the experimental results even without the assumption of interlayer coupling.

IV. CONCLUSIONS

We have presented the complete current response of the gapless semiconductor graphene due to coherent control of light at frequencies \(\omega\) and \(2\omega\). By considering the additional interference effect between stimulated ERS and 1PA of the fundamental, occurring with a net energy absorption of \(\hbar \omega\), we have shown that graphene presents a photoresponse sensitive to the relative orientation of the linear polarization axes of the light. This polarization sensitivity, characterized by a tunable disparity parameter \(-1 \leq d \leq 1/3\), is in stark contrast with the polarization-isotropic photocurrent contribution due to 1PA and 2PA interference alone.\(^8\) The value of \(d = 1/3\) for intrinsic graphene is closer to typical values in GaAs,\(^9\) and with a value of \(d = 0\) it is possible to completely suppress the current injection for perpendicular polarization axes. Thus, with its Fermi level adjustable through doping or electrical gating, graphene offers tunable, polarization sensitive applications.

While the additional interference term between stimulated ERS and 1PA is correctly included in a recent treatment of third-order nonlinear optical conductivities of doped graphene,\(^10\) it had not been carefully considered in previous studies of coherent optical injection and control in graphene and carbon nanotubes.\(^7\) However, we have shown that this term modifies the CC photocurrent response significantly, raising the question whether previous experimental results need to be reinterpreted.\(^8\)\(^,\)\(^10\)\(^,\)\(^12\) In experiments with fixed polarization the ERS contribution does not play a crucial role, specifically the conclusions of Newson et al. regarding CC using colinearly-polarized beams in carbon nanotubes,\(^9\) and those of Sun et al. using cross-polarized beams in multilayer epitaxial graphene,\(^10\)\(^,\)\(^13\) are not altered. Considering the ERS contribution and depending on the level of doping, cross-polarized beams could lead to counter-propagating currents in the undoped and heavily-doped layers of epitaxial graphene, an effect that is not resolvable in the employed THz detection technique. Such different response from the undoped and heavily-doped layers offers an alternative explanation for the polarization-resolved data of Sun et al.\(^12\) without involving the interlayer coupling.

Besides gapless semiconductors such as graphene, a careful treatment of the interference between stimulated electronic Raman scattering and linear absorption is important for the complete description of two-color coherent control in metals, topological insulators, and in semiconductors when \(\hbar \omega\) exceeds the bandgap.

ACKNOWLEDGMENTS

This work was supported by the Deutsche Forschungsgemeinschaft (DFG) under project number SFB 767 and the Konstanz Center for Applied Photonics (CAP). J.E.S. acknowledges funding from the National Sciences and Engineering Research Council of Canada. The authors acknowledge useful discussions with Jin Luo Cheng, Dong Sun and Ted Norris.

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