Photoemission study of the metal-insulator transition in VO$_2$/TiO$_2$(001) : Evidence for strong electron-electron and electron-phonon interaction

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We have made a detailed temperature-dependent photoemission study of VO$_2$/TiO$_2$(001) thin films, which show a metal-insulator transition at $\sim$ 300 K. Clean surfaces were obtained by annealing the films in an oxygen atmosphere. Spectral weight transfer between the coherent and incoherent parts accompanying the metal-insulator transition was clearly observed. We also observed a hysteretic behavior of the spectra for heating-cooling cycles. We have derived the “bulk” spectrum of the metallic phase and found that it has a strong incoherent part. The width of the coherent part is comparable to that given by band-structure calculation in spite of its reduced spectral weight, indicating that the momentum dependence of the self-energy is significant. This is attributed to ferromagnetic fluctuation arising from Hund’s rule coupling between different $d$ orbitals as originally proposed by Zylbersztejn and Mott. In the insulating phase, the width of the V 3$d$ band shows strong temperature dependence. We attribute this to electron-phonon interaction and have reproduced it using the independent boson model with a very large coupling constant.

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I. INTRODUCTION

To elucidate the physical properties of Mott-Hubbard systems has been one of the most challenging subjects in condensed matter physics and has continued to pose controversial theoretical as well as experimental issues. In this respect, the single-particle spectral function of transition-metal oxides, particularly of early transition-metal oxides, is of fundamental importance in the physics of Mott-Hubbard systems. In fact, the coexistence of the coherent part [the quasi-particle (QP) band] and the incoherent part (a remnant of the upper and lower Hubbard bands) in the spectral function and spectral weight transfer between them as a function of electron correlation strength $U/W$, where $U$ is the Coulomb repulsion energy and $W$ is the bandwidth, are a remarkable manifestation of electron correlation as identified in the photoemission spectra of V and Ti oxides. Theoretically, dynamical mean-field theory (DMFT) applied to the Hubbard model has successfully reproduced these characteristic features. Comparison between experiment and theory, however, has not been straightforward. In DMFT, the self-energy is necessarily local, and therefore the density of states (DOS) at the Fermi level ($E_F$), namely, the spectral intensity at $E_F$ remains the same as that of the non-interacting system and electron correlation effect manifests itself as the narrowing of the coherent QP band. Experimentally, the reduction of the DOS at $E_F$ rather than the narrowing of the coherent part was observed in the photoemission spectra of Ca$_{1-x}$Sr$_x$VO$_3$, suggesting the importance of the momentum dependence of the self-energy. However, a recent “bulk-sensitive” photoemission study of the same compounds has shown that the QP band is indeed narrowed and the DOS at $E_F$ remains unchanged from that predicted by band-structure calculation, indicating that the self-energy is nearly momentum-independent as assumed in DMFT. In the present work, we have studied another typical Mott-Hubbard system VO$_2$, which undergoes a metal-insulator transition as a function of temperature, and examined the spectral function of the “bulk” to see whether the self-energy is momentum-independent or not. Our results have shown that the self-energy is momentum-dependent, probably due to ferromagnetic fluctuations arising from the multi-orbital nature of the V 3$d$ band of the rutile structure.

VO$_2$ is well-known for its first-order metal-insulator transition (MIT) at 340 K. The transition is accompanied by a structural transition. In the high temperature metallic phase it has a rutile structure while in the low temperature insulating phase ($M_1$ phase) the V atoms dimerize along the $c$-axis and the dimers twist, resulting in a monoclinic structure. The magnetic susceptibility changes from paramagnetic to nonmagnetic in going from the metallic to the insulating phases. Hence, this transition is analogous to a Peierls transition and in fact the importance of electron-phonon interaction has been demonstrated by Raman scattering and x-ray diffraction studies. On the basis of local-density approximation (LDA) band-structure calculation, Wentzcovitch $et$ $al.$ concluded that the insulating phase of VO$_2$ is an ordinary band (Peierls) insulator. On the other hand, the magnetic susceptibility of the high-temperature metallic phase is unusually high and temperature dependent, indicating the importance of electron-electron correlation. Furthermore, Cr-doped VO$_2$ or pure VO$_2$ under uniaxial pressure in the [110] direction of the rutile structure has
another monoclinic insulating phase called \(M_2\) phase. In the \(M_2\) phase, half of the V atoms form pairs and the other half form zig-zag chains.\(^2\) While the V atoms in the pairs are nonmagnetic, those in the zig-zag chains have local moment and are regarded as one-dimensional Heisenberg chains according to an NMR study. Based on these observations for the \(M_2\) phase, Rice et al.\(^11\) objected Wentzcovitch et al.’s argument. Thus it still remains highly controversial whether the MIT of VO\(_2\) is driven by electron-phonon interaction (resulting in a Peierls insulator) or electron-electron interaction (resulting in a Mott insulator forming a spin-Peierls-like state).

To deal with the above problems, photoemission spectroscopy is a powerful technique and in fact has been extensively applied to this material.\(^12,13,14,15,16,17,18\) However, detailed photoemission studies of the MIT has been hampered because the transition temperature of bulk VO\(_2\) is rather high and therefore it is difficult to keep the surface clean in an ultra-high vacuum for the high-temperature metallic phase. Also, because the transition is strongly first-order with the structural change, the sample is destroyed when it crosses the MIT and one can go through the transition only once for one sample.

In this work, we have avoided those experimental difficulties by using thin film samples epitaxially grown on TiO\(_2\)(001) surfaces using the pulsed laser deposition technique.\(^19\) After having obtained a clean surface by oxygen annealing, the surface remained fairly stable for several hours even in the high-temperature metallic phase and allowed us to study detailed temperature-induced changes both in the metallic and insulating phases including the hysteretic behavior across the MIT. Spectral weight transfer between the coherent and incoherent parts of the V 3\(d\) spectral function accompanying the metal-insulator transition was clearly observed. We have attempted to deduce the “bulk” photoemission spectrum by subtracting surface contributions from the measured spectra. We compare the “bulk” spectrum with the band-structure calculation to discuss electron correlation in the metallic phase, particularly possible momentum dependence of the self-energy. We have also found a strong temperature dependence in the spectra of the insulating phase and attributed it to strong electron-phonon interaction.

\section{II. EXPERIMENTAL}

VO\(_2\)/TiO\(_2\)(001) thin films were prepared using the pulsed laser deposition technique as described in Ref.\(^19\). A V\(_2\)O\(_3\) pellet was used as a target. During the deposition, the substrate temperature was kept at 733 K and oxygen pressure was maintained at 1.0 Pa. The film thickness was about 10 nm. The epitaxial growth was confirmed by four-cycle x-ray diffraction (XRD) measurements and the MIT was confirmed by electrical resistivity measurements showing a jump of about three orders of magnitude. The transition temperature in the films was 295 K on heating cycle and 285 K on cooling cycle, while the MIT occurs at 340 K in bulk samples.\(^2\) The reduced MIT temperature of the films is due to the compressive strain from the TiO\(_2\) substrate.\(^2\) Bulk VO\(_2\) single crystals were prepared by the chemical vapor transport method and measured as described in Ref.\(^18\).

X-ray photoemission spectroscopy (XPS) and ultraviolet photoemission spectroscopy (UPS) measurements were performed using the Mg K\(\alpha\) line (\(h\nu = 1253.6\) eV) for XPS and the He I resonance line (\(h\nu = 21.2\) eV) for UPS with a VSW hemispherical analyzer. Estimation of the instrumental resolution and binding energy calibration were made by measuring gold spectra. The total energy resolution was \(\sim 0.8\) eV for XPS and \(\sim 30\) meV for UPS. Clean surfaces were obtained by annealing the films in a preparation chamber connected to the spectrometer at 643 K under \(\sim 1\) Pa oxygen atmosphere for 1 hour prior to the photoemission measurements.

\section{III. RESULTS}

Figure 1 shows the O 1\(s\) and V 2\(p\) core-level XPS spectra of VO\(_2\)/TiO\(_2\)(001) film taken at room temperature. Contributions from the Mg K\(\alpha_3\) and K\(\alpha_4\) satellites have been subtracted. The O 1s peak shows a single peak without any contamination signals at higher binding energies, indicating that the surface became sufficiently clean by the above procedure.

Figure 2 shows the valence-band UPS spectra of VO\(_2\)/TiO\(_2\)(001) taken at 300 K and 280 K. The secondary electron background has been subtracted following the procedure of Li and Henrich.\(^20\) The structures from binding energies \(E_B \approx 2\) to 12 eV are due to the O 2\(p\) band. The region from \(E_B \approx 2\) eV to \(E_F\) is the V 3\(d\) band. While the O 2\(p\) band shows no clear temper-

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{fig1.png}
\caption{O 1\(s\) and V 2\(p\) core-level XPS spectra of VO\(_2\)/TiO\(_2\)(001) thin film.}
\end{figure}
Intensity (arb. units) vs. Binding Energy (eV) for VO$_2$/TiO$_2$(001) thin film. Secondary electron background has been subtracted.

At room temperature, the V 3d band shows a temperature dependence, indicating that the MIT occurred between 280 and 300 K.

Figure 3 (a) and (b) shows the UPS spectra of VO$_2$/TiO$_2$(001) in the V 3d band region taken at various temperatures. First, the temperature was decreased from 300 K to 150 K, then it was increased again to above 300 K. The spectra showed good reproducibility within this temperature cycle. The tail of the O 2p band has been subtracted as shown in Fig. 3 (a) and the resulting spectra have been normalized to the integrated intensity from $E_B = -0.3$ to $2.3$ eV, as shown in Fig. 3 (b). The MIT is clearly seen as the change in the spectral intensity at $E_F$ accompanied by the spectral weight transfer between the low binding-energy region $E_B = 0.5$-2 eV (coherent part) and the high binding-energy region $E_B = 0.5-2$ eV (incoherent part). The spectra of the films (Fig. 3(b)) are almost identical to that of the bulk sample (Fig. 3(c)) except for the somewhat stronger temperature dependence of the film spectra. Because of the much higher stability of the film surface in vacuum, we could obtain the spectra with much higher signal-to-noise ratio at much smaller temperature intervals in the whole temperature range. Also, the film retained the original spectra after several temperature cycles whereas the bulk single crystal broke into pieces once it crossed the MIT. In the previous study of bulk single crystals, detailed temperature-dependent studies were therefore limited to the low-temperature insulating phase, where the crystal did not break. The present temperature dependence in the insulating phase has reproduced the bulk crystal results.

Here, we have observed a hysteretic behavior in the spectra with temperature across the MIT, as demonstrated by the temperature dependence of the intensity around $E_F$ (integrated from $E_B = -0.2$ to 0.5 eV) shown in the inset of Fig. 3(b). The hysteretic behavior is seen over the temperature range of $\sim 10$ K. This may indicate the co-existence of metallic and insulating regions with changing volume fractions in this temperature range. Photoemission spectra of another system which shows a first-order temperature-induced metal-insulator transition, RNiO$_3$, also shows a similarly gradual temperature dependence. In the case of RNiO$_3$, the hysteretic behavior in the transport and thermodynamic properties extends over a wide temperature range of several tens K, and correspondingly the photoemission spectra show a more gradual temperature dependence over the wider temperature range.

Recently, it has been demonstrated that photoemission spectra of transition-metal oxides are strongly influenced by surface contributions. In particular, the incoherent part centered around $E_B = 1-1.5$ eV contains more...
raw data
20% subtracted
25% subtracted
33% subtracted
40% subtracted
50% subtracted

VO$_2$/TiO$_2$(001)

(a) T = 350 K

raw data
20% subtracted
25% subtracted
33% subtracted
40% subtracted
50% subtracted

(b) XPS

FIG. 4: (a) Subtraction of “surface” contributions with various ratios from the photoemission spectrum of the metallic phase. (b) Comparison of the spectra in (a) with the XPS spectrum from Ref. 12. Here, the curves in (a) have been broadened with a Gaussian to account for the lower energy resolution of XPS.

surface contributions than the coherent part. Since the surface layer tends to have a smaller bandwidth $W$ and hence a larger $U/W$, the surface layer tends to have stronger incoherent part and weaker coherent part than in the bulk. In order to remove such surface contributions and to analyze the electronic structure of bulk materials, we attempted to deduce the “bulk” spectrum in the metallic phase under several assumptions. If the thickness of the surface layer is $d$ and the photoelectron escape depth is $\lambda$, the observed spectrum $F(\omega)$ is given by

$$F(\omega) = F^s(\omega)(1 - e^{-d/\lambda}) + F^b(\omega)e^{-d/\lambda}, \quad (1)$$

where $F^s(\omega)$ and $F^b(\omega)$ are the “surface” and the “bulk” spectra, respectively. As the electronic properties of the surface layer of VO$_2$ are not precisely known, in the following analyses, we consider the extreme case where the photoemission spectra of the surface layer largely consists of the incoherent part. Therefore, the intensity of the incoherent part in the “bulk” spectrum deduced below should be regarded as the lower bound for the actual bulk one.

Assuming that the spectrum at 280 K ($< T_{MI}$) represents the “surface” spectrum, because the photoelectron escape depth $\lambda$ is not precisely known, we subtracted the “surface” contribution with various ratios as shown in Fig. 4 (a). Here, “20% subtracted” means that the intensity of the subtracted insulator-like spectrum was 20% of the total intensity. In Fig. 4 (b), we compare the “bulk sensitive” XPS spectrum in the literature with those spectra in (a) after having broadened them with a Gaussian function corresponding to the lower experimental energy resolution of XPS ($\sim 0.55$ eV). One can see that the XPS spectrum is in best agreement with “20% subtracted” spectrum. According to the “universal curve” of the photoelectron escape depth, the escape depth is $\sim 10$ Å for $h\nu = 21.2$ eV and $\sim 15$ Å for XPS ($h\nu = 1486.6$ eV), respectively. Using the surface layer thickness of $2c (= 5.7$ Å) on the (001) surface of the rutile structure, where $c$ is the $c$-axis lattice constant, the surface contribution is $\sim 44\%$ for $h\nu = 21.2$ eV and $\sim 32\%$ for $h\nu = 1486.6$ eV, respectively. Hence, the “20% subtracted” spectrum should have 30% surface contribution and therefore it is reasonable that the “20% subtracted” spectrum is in agreement with the XPS spectrum. After all, we consider that the “bulk” spectrum is given by the “40% subtracted” spectrum.

IV. DISCUSSION

A. Metallic phase

In Fig. 5, we compare the “bulk” spectrum thus deduced with the LDA band-structure calculation. The calculated density of states (DOS) is multiplied by the Fermi-Dirac distribution function at 350 K and broad-
ened with a Gaussian corresponding to the instrumental energy resolution. The width of the coherent part \( \sim 0.5 \) eV is similar to that given by the band-structure calculation. This means that \( m^*/m_b \) is \( \sim 1 \), where \( m^* \) is the average effective mass of the QP and \( m_b \) is the average bare band mass of the V 3d band. From the spectral weight ratio of the coherent part to the incoherent part, 1 : 2, the renormalization factor becomes \( Z \sim 1/3 \). From the ratio of the intensity at \( E_F \) of the spectra to the DOS given by the band-structure calculation, one can estimate the average \( k \)-mass defined by \( m_k/m_b = \frac{\partial^2 \epsilon}{\partial k^2} |_{k=k_F} / \frac{\partial \epsilon}{\partial k} |_{k=k_F} \), as \( m_k/m_b \sim 0.3 \). Thus, we again obtain \( m^*/m_b = (1/Z) (m_k/m_b) \sim 1 \). Note that we have assumed that the surface layer is without the coherent part around \( E_F \). If the surface spectrum has a finite coherent part, the coherent part of the “bulk” spectrum would be further reduced and the deduced \( k \)-mass would be even smaller. Hence, \( m_k/m_b \sim 0.3 \) deduced here should be taken as the upper limit for \( m_k/m_b \), and therefore on can safely conclude the \( m_k/m_b \) is smaller than unity. That is, the momentum dependence of the self-energy is not negligible in the metallic phase of VO2.

Our finding \( m_k/m_b < 1 \) is contrasted with the “bulk” spectra of \( Sr_{1-x}Ca_xVO_3 \) reported by Sekiyama et al. In their result, the width of the coherent part of the V 3d band of SrVO3 is reduced by a factor of \( \sim 40 \% \) compared with the LDA result, and the spectral weight of the coherent part is also reduced by \( \sim 40 \% \) due to the transfer of spectral weight to the incoherent part, resulting in almost the same spectral intensity at \( E_F \) as that of the LDA value, that is, the self-energy has negligible momentum dependence in \( Sr_{1-x}Ca_xVO_3 \). The origin of the momentum dependence of the self-energy in VO2 is not known at this moment. One possibility is poor screening of long-range Coulomb interaction, but it is unlikely that the screening effect is so different between VO2 and \( Sr_{1-x}Ca_xVO_3 \). Another possible origin of the momentum dependence is ferromagnetic fluctuations in VO2 considering the enhanced magnetic susceptibility in the metallic phase, corresponding to \( m^*/m_b \sim 6 \) (Ref. 23). Recently, Liebsch and Ishida proposed that the multi-orbital nature of the V 3d band is important to describe the metallic phase of VO2 (Ref. 28,30), following the idea originally proposed by Zylbersztejn and Mott. According to these works, the occupancy of the \( t_{2g} \) orbitals is very different between the metallic and the insulating phases due to lattice distortion in the insulating phase and this affects the role of local Coulomb interaction in each phase. If many orbitals contribute to the metallic conductivity, ferromagnetic correlation may arise from Hund’s coupling between those orbitals. Further studies are necessary to confirm this scenario.

B. Insulating phase

As stated in Sec. 11 it has been controversial whether the insulating band gap is primarily caused by the lattice distortion or the electron-electron interaction. In order address this issue, it is useful to examine the photoemission spectral line shape of the V 3d band in the insulating phase.

In Fig. 6 we compare the UPS spectrum of the insulating phase with the DOS given by the LDA+U band-structure calculation (\( U = 4.0 \) eV) by Huang et al.22 where the effect of electron-electron interaction is taken into account on the mean-field (i.e. Hartree-Fock) level. The figure shows that, although the insulating gap can be produced by the LDA+U method, the Gaussian-like broad spectrum of V 3d band cannot be reproduced. This disagreement between theory and experiment cannot be explained by a surface effect because since the bulk component should have finite contribution (\( \sim 60 \% \)) even for this low photon energy and therefore the sharp feature should be clearly visible overlapping the surface signals. This means that electron-electron interaction on the mean-field level is not sufficient to understand the photoemission spectrum of the insulating VO2. Here, we point out that the photoemission spectra of a double-layer manganite \( La_{1.2}Sr_{1.8}Mn_2O_7 \) also show a broad Gaussian-like line shape in striking contrast with LDA band-structure calculation, and this discrepancy has been attributed to the strong electron-phonon coupling. Furthermore, one can recognize that the spectra of VO2 show very strong temperature dependence in the insulating phase as shown in Fig 3. The same temperature dependence was observed in the spectra of bulk single crystal and was attributed to electron-phonon interaction, because the core-level spectra also show a similarly strong temperature dependence.18

Simple thermal broadening cannot explain the observed temperature dependence as shown in Fig. 4(a), where the photoemission spectrum taken at 150 K and the same spectrum broadened with a Gaussian, whose
FWHM is 200 meV (∼ 8k_BT at 300 K) are compared. In order to simulate the temperature-dependence based on the electron-phonon interaction mechanism, we introduce the spectral function of the independent boson model at finite temperature given by

\[ A(\omega) = e^{-g(2N+1)} \sum \frac{g^l}{l!} \sum \frac{C_m N^m (N+1)^{l-m}}{l-2m} \cdot \delta(\omega - \varepsilon_c + \Delta - (l-2m)\omega_0), \]

where \( N \) is the phonon occupation number, \( g \) is the electron-phonon coupling constant, \( \omega_0 \) is the average phonon energy, the \( \Delta = g\omega_0 \) is the electron self-energy shift due to coupling to phonons and \( \varepsilon_c \) gives the peak position of the spectra. This spectral function describes the situation where spectral weight is transferred from the zero-phonon line at the lowest binding energy \( \varepsilon_c - \Delta \) to \( \varepsilon_c - \Delta + (l-2m)\omega_0 \) by emitting \( (l - m) \) phonons or absorbing \( m \) phonons. Because this spectral function consists of a series of delta functions, one has to broaden this function to compare with the photoemission spectra. For this purpose, we use a simplified model self-energy \( \Sigma(\omega) = G \omega / (\omega + i\gamma)^2 \), which simulates the “life time” broadening which increases with increasing binding energy. In Fig. 7 (b) and (c), we compare the spectral function of the independent boson model with the photoemission spectra of VO_2/TiO_2(001) in the insulating phase. We have chosen the parameters as \( \varepsilon_c = 1.2 \) eV, \( g = 40 \) and \( \omega_0 = 0.03 \) eV (Ref. 30) for the independent boson model and \( G = 1.5 \) eV^2 and \( \gamma = 2 \) eV for the broadening. Because the tail of the lower binding energy side of the photoemission spectrum reaches the vicinity of \( E_F \), we have chosen the coupling constant \( g \) so that \( \varepsilon_c - \Delta \approx 0 \). Hence, \( g = \varepsilon_c / \omega_0 \approx 40 \). One can see that the temperature-dependent spectral function of the independent boson model qualitatively reproduces the photoemission spectra.

The extremely large coupling constant \( g = 40 \) may appear unphysical at first sight. However, Citrin et al. have shown that in ionic crystals the coupling constant can be large and reported \( g = 55 \) for KI based on their analysis of temperature-dependent core-level photoemission spectra. They have estimated the value of \( g \) using the expression \( g = e^2 (6/\pi V)^{1/3} (1/\varepsilon_{\infty} - 1/\varepsilon_0) / \omega_0 \), where \( V \) is the volume of a primitive unite cell, \( \varepsilon_{\infty} \) and \( \varepsilon_0 \) are the high- and low-frequency limits of the dielectric constant. For VO_2, \( V \sim 29.5 \) Å^3, \( \varepsilon_{\infty} \) and \( \varepsilon_0 \) have been given as 5 and 30 in Ref. 31, respectively. From these values, \( g \) is calculated as \( \sim 32 \). On the other hand, Egdell et al. have used \( 1/2R \) in stead of \( (6/\pi V)^{1/3} \) for perovskite-type V oxides, where \( R \) is the ionic radius of the transition-metal ion. In this case, \( g \) becomes as large as 47. \( (R \) is 0.82 Å for VO_2) Hence, we can say that \( g = 30 - 50 \) is a reasonable value for the electron-phonon coupling constant for VO_2.

Finally, we comment on how the strong electron-electron interaction and the strong electron-phonon coupling are related with each other in VO_2 (and probably in other transition-metals as well). In ionic crystals, the on-site Coulomb repulsion energy \( U \) is given by \( U = e^2 / 2\varepsilon_{\infty} R \). Therefore, according to Egdell et al.’s expression 38 the large \( U \) and the large \( g \) is related with each other though \( \varepsilon_{\infty} \). This means that the strong electron-phonon interaction is a consequence of strong electron-electron interaction.

V. CONCLUSION

We have studied the electronic structure of VO_2 by measuring the photoemission spectra of VO_2/TiO_2(001)
thin films. The metal-insulator transition was clearly observed as a change in the spectral intensity at $E_F$ accompanied by spectral weight transfer between the coherent and incoherent parts of the spectral function. From comparison of the “bulk” spectrum in the metallic phase and the band-structure calculation, we have concluded that, while the mass enhancement factor $m^*/m_b$ is almost unity, the momentum dependence of the self-energy is important in the metallic phase, possibly due to ferromagnetic fluctuations arising from the multi-oriatal character of the V 3d band. In the insulating phase, the V 3d band is strongly broadened as the temperature is increased. We attribute this temperature dependence to the electron-phonon interaction and reproduced it using the independent boson model with a very large coupling constant. This indicates that, while electron-electron interaction is necessary to produce the band gap in the insulating phase, electron-phonon interaction is important to fully understand the electronic structure and charge transport in VO$_2$.

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