Spectral features in isolated neutron stars induced by inhomogeneous surface temperatures

Daniele Viganò, Rosalba Perna, Nanda Rea and José A. Pons

1 Institute of Space Sciences (CSIC–IEEC), Campus UAB, Faculty of Science, Torre C5-parell, E-08193 Bellaterra, Spain
2 Department of Physics and Astronomy, Stony Brook University, Stony Brook, NY 11794, USA
3 Astronomical Institute 'Anton Pannekoek', University of Amsterdam, Postbus 94249, NL-1090GE Amsterdam, the Netherlands
4 Departament de Física Aplicada, Universitat d’Alacant, Ap. Correus 99, E-03080 Alacant, Spain

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ABSTRACT
The thermal X-ray spectra of several isolated neutron stars display deviations from a pure blackbody. The accurate physical interpretation of these spectral features bears profound implications for our understanding of the atmospheric composition, magnetic field strength and topology, and equation of state of dense matter. With specific details varying from source to source, common explanations for the features have ranged from atomic transitions in the magnetized atmospheres or condensed surface, to cyclotron lines generated in a hot ionized layer near the surface. Here, we quantitatively evaluate the X-ray spectral distortions induced by inhomogeneous temperature distributions of the neutron star surface. To this aim, we explore several surface temperature distributions, we simulate their corresponding general relativistic X-ray spectra (assuming an isotropic, blackbody emission), and fit the latter with a single blackbody model. We find that, in some cases, the presence of a spurious 'spectral line' is required at a high significance level in order to obtain statistically acceptable fits, with central energy and equivalent width similar to the values typically observed. We also perform a fit to a specific object, RX J0806.4−4123, finding several surface temperature distributions able to model the observed spectrum. The explored effect is unlikely to work in all sources with detected lines, but in some cases it can indeed be responsible for the appearance of such lines. Our results enforce the idea that surface temperature anisotropy can be an important factor that should be considered and explored also in combination with more sophisticated emission models like atmospheres.

Key words: stars: neutron – X-rays: stars.

1 INTRODUCTION
Isolated neutron stars (NSs) display an observational variety of timing and spectral properties which has led, historically, to a classification in different subclasses. Rotation-powered pulsars (RPPs, Becker 2009) constitute the majority of known pulsars; they convert part of their rotational energy into non-thermal radiation across the whole electromagnetic spectrum. More than 2000 sources are visible in radio, and more than 100 in X-rays and/or γ-rays. Other NSs are detected only or mostly in X-rays: ~20 magnetars (Mereghetti 2008), the seven nearby thermally emitting NSs (simply named XINSs; Turolla 2009) and the handful of heterogeneous central compact objects (CCOs, Gotthelf, Halpern & Alford 2013).

In about 40 of the pulsars visible in X-rays, the spectrum shows evidence for thermal emission (see Viganò et al. 2013 and our website1 for a catalogue). Therefore, the X-ray spectra carry precious information about the surface properties and the physics of the crust. However, the ability to draw firm implications from the analysis of the properties of the thermal emission is often hampered by the faintness of some objects, the co-existence of different physical mechanisms contributing to the detected radiation (rotation-powered non-thermal radiation in RPPs, and magnetospheric Compton scattering in magnetars), and the presence of interstellar absorption.

The temperatures inferred from blackbody (BB) fits to X-ray spectra range from $kT_{bb} \sim 45–100$ eV (in XINSs and some standard radio pulsars), up to 300–500 eV in some magnetars (during their quiescent state). The inferred radii are also systematically smaller.

* E-mail: vigano@ice.cat

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1 www.neutronstarcooling.info
than the typical 10–12 km expected from an NS. In some cases, e.g. the three musketeers (De Luca et al. 2005), the CCO in Puppis A (Gotthelf, Perna & Halpern 2010; de Luca et al. 2012), and a few magnetars (Halpern & Gotthelf 2005; Bernardini et al. 2009, 2011; Albano et al. 2010), phase-averaged and phase-resolved spectra can be modelled by considering spectral models with two or three temperatures, physically interpreted as coming from different regions of the star surface.

Other objects, and in particular the XINSs, display a spectrum which is often broadly consistent with a single-temperature model. However, when the source is observed at a sufficiently high signal-to-noise, deviations are seen, often in the form of a feature in the spectrum.

Deviations from a pure BB spectrum can be produced by several physical effects. First, the presence of a thin atmospheric layer (Romani 1987; van Riper 1988; Miller 1992; Pavlov et al. 1995; Zavlin, Pavlov & Trumper 1998; Ho & Lai 2001; Özel 2001; Ho & Lai 2003a,b; Ho et al. 2003; Mori & Hailey 2006; van Adelsberg & Lai 2006; Suleimanov, Potekhin & Werner 2009; Suleimanov, Pavlov & Werner 2010, 2012) distorts and broadens the spectrum. The (poorly known) chemical composition of the atmosphere and the degree of ionization of the species, the strong magnetic field, the vacuum polarization effect, all introduce various distortions and features in the resulting spectra. Also, as an alternative to atmospheres, condensed surface models have been proposed (van Adelsberg et al. 2005; Pérez-Azorín et al. 2006), and could be particularly suitable for strongly magnetized objects, in which the outer layers consist of atomic chains (Chen, Ruderman & Sutherland 1974). Hybrid models, with a condensed surface covered by a thin atmosphere, have been proposed to explain the optical to X-ray spectra of the XINS RX J1856.5–3754 (Ho et al. 2007; Ho 2007).

Spectral features in the spectra can be produced by proton and electron cyclotron emission/absorption at harmonics of the cyclotron frequency, and by electronic transitions in neutral and partially ionized atoms (Sanwal et al. 2002; van Kerkwijk et al. 2004; Suleimanov et al. 2012). However, at high magnetic fields, $B \gtrsim 10^{12}$ G, vacuum polarization tends to reduce the contrast of those spectral features (Ho & Lai 2003b).

Spectral distortions from a pure BB are expected also as a result of an inhomogeneous temperature distribution on the NS surface. Such temperature inhomogeneities can be inferred from measurements of small emitting BB areas in a number of isolated NSs (e.g. Halpern & Gotthelf 2010), and are theoretically predicted, e.g. by anisotropic thermal conductivity induced by the presence of strong magnetic fields (e.g. Page, Geppert & Küker 2007; Pons, Miralles & Geppert 2009), and by magnetospheric particle bombardment (Cheng & Ruderman 1980).

In this work, we perform a general study of the resulting spectral features arising from different surface temperature distributions. In the spirit of focusing on this effect only, and of separating its contribution from the other effects discussed above, we consider a local isotropic BB emission; however, the same concept could be applied to more sophisticated emission models. We note that our study is of relevance to the cases in which the spectral feature is detected in the thermal part of the spectrum, and when it is relatively broad.

For the purpose of our investigation, we consider several representative axisymmetric surface temperature distributions, we numerically compute their general relativistic spectra (both phase-averaged and phase-resolved), and we use them to simulate ‘observational’ data. We then fit these synthetic spectra with a BB model and a BB plus an absorption line model, and we explore the conditions under which the presence of a ‘spurious line’ in the spectra is required at high significance in the simulated spectra. We then consider the actual XMM–Newton data for a particular source, RX J0806.4–4123, for which an absorption line has been claimed in the spectrum. We show that it is possible to find several temperature profiles which provide a good overall fit to the observed spectral distribution.

This paper is organized as follows: in Section 2, we review the literature on absorption features in NS X-ray spectra. In Section 3, we present the considered axisymmetric surface temperature distributions, and calculate the corresponding general-relativistic spectra. In Section 4, we compute synthetic spectra from the theoretical ones, and discuss the fit results to these synthetic spectra when modelled with a BB and a BB plus an absorption line. We further present the results of the fit to RX J0806.4–4123. Finally, we discuss and summarize our results in Section 5.

2 OBSERVED SPECTRAL FEATURES

In Table 1, we list the reported broad spectral features in isolated neutron stars (XINSs, CCOs, RPPs, magnetars). Most of the reported cases resulted from the analysis of XMM–Newton/EPIC-pn data, thanks to its large effective area.²

The XINSs are seven nearby, middle-aged (~10⁵–10⁶ yr), and slowly rotating NSs. Their surface X-ray emission is not reprocessed by a dense magnetospheric plasma (as in magnetars) or contaminated by rotationally-powered non-thermal photons (as in RPPs); also, since they are nearby objects, they suffer little interstellar absorption ($N_{\text{H}} \sim 10^{20} \text{ cm}^{-2}$). As a consequence, the XINSs are the ideal candidates to study the NS surface emission properties. Their deepest observations have collected ~10⁵–10⁶ photons, most of which at low energy (below 1 keV), and with a spectral distribution well described by a thermal component. The bright source RX J1856.5–3754 is compatible with a perfect BB (Burwitz et al. 2003), with hints for a second cold component (Sartore et al. 2012), detected also in optical and ultraviolet analyses (Pons et al. 2002). For the faint source RX J0420.0–5022, the initial claims for a line (Haberl et al. 2004b) were not confirmed by later, deeper observations (Kaplan & van Kerkwijk 2011).

For the other XINSs, small deviations from perfect Planckian spectra appear ubiquitously (Haberl et al. 2003, 2004b; van Kerkwijk et al. 2004; Zane et al. 2005; Haberl et al. 2006). RX J1308.6+2127 shows the deepest spectral feature among the XINSs, while in RX J0806.4–4123 and RX J1605.3+3249, hints of weak spectral features appear at ~300–400 eV. In XINSs, the width of the Gaussian lines, $\sigma$, is generally ~70–170 eV, while the equivalent width, $W_{\text{eq}}$, ranges between ~30 and 150 eV. Note that the five XINSs with claims for lines have similar temperatures, $kT_{\text{bb}} \sim 80–100$ eV, while the remaining two objects (with no apparent spectral features) are the coldest ones, with $kT_{\text{bb}} \sim 45–60$ eV. Given the strength of the dipolar magnetic fields of the XINSs, the physical origin of these features has been proposed to be cyclotron absorption by protons.

CCOs are X-ray bright objects observed in the centre of young supernova remnants (SNRs), a class that is possibly comprising a few diverse objects. The bright CCO 1E 1207.4–5209 exhibits a

² Hohle et al. (2012a), by using the spectrometer XMM–Newton/RGS, found several very narrow features in nearby NSs, whose origin could also be due to absorption by the interstellar medium. We do not consider these features here, since they are too narrow and cannot be produced by an inhomogeneous temperature distribution.
complex spectrum, phenomenologically fitted by a purely thermal continuum, plus several very broad absorption lines. The central energies $E_0$ of these features have been interpreted as the fundamental and upper harmonics of the cyclotron absorption by electrons.

Among the radio pulsars, the only two cases with reported absorption lines are PSR J1740+1000 (Kargaltsev et al. 2012), and the peculiar, highly magnetized rotating radio-transient PSR J1819–1458 (McLaughlin et al. 2007; Miller et al. 2013), at slightly higher energies than what observed in XINS, and similarly interpreted as cyclotron absorption lines.

Among the most strongly magnetized pulsars, a few claims are present in the literature, all tentatively interpreted as proton cyclotron absorption lines. They were observed either in the persistent emission (Rea et al. 2003, but see also Rea et al. 2005), or during bursts and outbursts (Ibrahim, Swank & Parke 2003; Tiengo et al. 2013), when the hard non-thermal emission is enhanced. In these cases, the features lie in the non-thermal part of the spectrum, thus they are not considered in this work. Only in one magnetar, XTE J1810–197 (Bernardini et al. 2009), the claimed feature is in a thermally dominated part of the spectrum, at an energy of $E_0 \sim 1.1$ keV. The best-fitting continuum model in this case is a complex 3BB line; however, it can also be modelled by a BB distorted by magnetospheric resonant cyclotron scattering (Rea et al. 2008).

### 3 SYNTHETIC SPECTRA

#### 3.1 Inhomogeneous temperature maps

The coupled internal evolution of magnetic field and temperature in the NS crust leads to inhomogeneous internal and surface temperatures under the presence of strong magnetic fields. Magnetic fields in NSs have often been approximated as dipolar; for this configuration, the equator, where the magnetic field is tangential, is colder than the rest of the NS surface, and the resulting temperature distribution is symmetric with respect to the equator. However, in reality the magnetic topology is likely to be much more complicated; in particular, toroidal and multipolar internal fields are likely to play an important role for at least a fraction of NSs. Strong dipolar toroidal fields break the symmetry with respect to the equator, and produce temperature distributions which yield small BB radii in spectral fits (Perna et al. 2013). The magnetothermal simulations by Pons et al. (2009) and Viganò et al. (2013) have shown that the temperature distribution is very sensitive to the details of the field geometry, which in turn depends to a significant extent upon the poorly known initial conditions at NS birth. Furthermore, small portions of the surface are believed to be kept hot by the particle bombardment from returning magnetospheric currents (rotationally powered for cold, middle-aged and old pulsars, Cheng & Ruderman 1980; Halpern & Ruderman 1993; Zavlin & Pavlov 2004, or magnetically powered in twisted magnetosphere of magnetars, Beloborodov 2013).

Given the theoretical uncertainties discussed above, it is not possible to make specific predictions for what the temperature distribution on the NS surfaces should be, and each case needs to be studied on its own. Therefore, for the general study of this work, we have opted to explore a variety of prescribed surface temperature profiles, without discussing their particular physical origin. In order to build them, we have used the most updated envelope models (used in Viganò et al. 2013 and adapted from Pons et al. 2009), with prescribed values of crustal temperature and magnetic field. In Fig. 1, we show some of the models studied in detail. The (unredshifted) surface temperatures of all these models are in the typical range $\sim 10^{3}$-300 eV. For simplicity, we divide the models into three families. Family A, shown in the left-hand panel, shows anisotropies qualitatively expected from NSs with crustal temperatures of $\sim 0.6-4 \times 10^{6}$ K, and surface magnetic field $\sim 10^{13}$ G. Families B (middle) and C (right) add a small hotspot to models from A; such localized heated regions could have a variety of physical origins (i.e. particle bombardment, twisted magnetic bundles), as mentioned above.
3.2 Ray tracing and phase-dependent spectra

The general relativistic, phase-dependent spectra are calculated using the formalism developed by Page (1995). Due to light deflection by the gravitational field of the star, a photon emitted at an angle $\delta$ with the normal to the NS surface will reach the observer if generated at an angle (with respect to the viewing axis)

$$\theta_v(\delta) = \int_0^{\frac{2\pi}{x}} x \left(1 - \frac{R_s}{R} \right) \left(1 - \frac{R_s}{2R} \right)^2 - (1 - 2\mu)x^2 \right)^{-1/2} \, dx,$$

where $x = \sin \delta$, $R_s = 2GM/c^2$ is the Schwarzschild radius of the star, and $M$ and $R$ are its mass and radius, respectively. In this work, we employ $M = 1.4 \, M_\odot$ and $R = 10$ km, yielding a gravitational redshift $(1 - R_s/R)^{1/2} = 0.766$. The radius measured by a distant observer would be $R_\infty = R/(1 - R_s/R)^{1/2} = 13$ km.

As the star rotates with angular velocity $\Omega(t)$, the observer measures the modulated photon flux

$$F(E_\infty, \alpha) = \frac{E_\infty^2}{c^2h^2D^2} \int_0^1 \int_0^{2\pi} I(\theta_v, \phi_v, E) \, d\phi_v \, dx,$$

where $D$ is the distance, $E_\infty = E(1 - R_s/R)^{1/2}$ is the energy measured by a distant observer, the spectral function $I(\theta_v, \phi_v, E)$ describes the dimensionless distribution of the locally emitted photons, and $(\theta_v, \phi_v)$ are the coordinates on the surface relative to the line of sight. Here, we assume the local emission to be isotropic and corresponding to a BB distribution with temperature $T(\theta_v, \phi_v)$, i.e. $I = (e^{E/T} - 1)^{-1}$.

The temperature distributions are assumed to be axisymmetric (see Fig. 1), and the magnetic axis is taken to coincide with the axis of symmetry of the temperature distribution. If we indicate by $\psi$ and $\xi$ the angles that the rotation axis makes, respectively, with the line of sight and the magnetic axis, then the angle between the line of sight and the magnetic axis, $\alpha$, is given by the simple geometric relation

$$\alpha(t) = \arccos \left[ \cos \psi \cos \xi + \sin \psi \sin \xi \cos \gamma(t) \right],$$

where $\gamma(t) = \int \Omega(t) \, dt$ is the phase angle swept by the star during its rotation (see Fig. 1 in Perna & Gotthelf 2008 for a graphical representation of the viewing geometry). From equation (2), the phase-averaged spectrum can be readily computed as an integral over the phase angle $\gamma$. For simplicity, we focus our analysis on spectra computed with $\psi = \xi = 90^\circ$ (orthogonal rotator), while briefly discussing the effects of the viewing geometry on the presented results.

4 SIMULATED SPECTRA AND FIT RESULTS

We imported the numerical, general relativistic spectra computed with the various temperature distributions into XSPEC, as tabular models. We then simulated synthetic observed spectra, using XMM-Newton/EPIC-pn response matrices in the fakeit procedure. For each model, we fixed the exposure time to be long enough to obtain a number of photons that would allow us to detect possible spectral features.

Phenomenologically, the spectra of isolated NSs showing spectral lines in their thermal emission are typically fitted by a model composed of a thermal component (BB or atmosphere) plus a phenomenological absorption model (gabs, gaua, cyclda) in the fitting package XSPEC (Arnaud 1996). When a phase-resolved spectral analysis is doable, spectral features can show phase-dependence (e.g. De Luca et al. 2004; Hambaryan et al. 2011; Kargaltsev et al. 2012).

For each simulated spectrum, we proceeded to the spectral analysis in the standard way, considering energies between 0.1 and 10 keV. We fitted the simulated spectra with two models: (a) BB, (b) BB+line (bbodyrad*gabs model in XSPEC), with the Gaussian width, $\sigma$, fixed to a given value. Freezing $\sigma$ is a standard way to proceed also in real observations (see e.g. Haberl et al. 2004b) when broad, weak features are present. As expected (see also Perna et al. 2013), the spectra from nearly uniform temperature distributions are always well fitted by a single BB. For conciseness, we do not discuss the trivial cases in detail. Hereafter we focus on the most interesting configurations for our purpose, i.e. those showing large temperature differences (at least a factor of ~ 2) between the coldest and the hottest regions (see Fig. 1).

We evaluated the systematic improvement in the fits obtained with the BB+line model with respect to the pure BB, by looking at the shape of the residuals and the values of $\chi^2$ (normalized by the number of degrees of freedom) for the different realizations. We confirmed the robustness of the results by finding, for each model, the systematic appearance of a spurious line with similar parameters in tens of different simulations. By computing the contribution to the flux of lines and continuum, we can also estimate the equivalent width of the line, $E_{\lambda}$. The latter, both in observations and in our simulations, is typically tens or hundreds of eV.

However, note that equally good fits can often be found for similar values of $E_{\lambda}$ but different values of $\sigma$ (varying by factor of a few), or different line models (gabs, gaua, cyclda). Since this variability strongly affects the equivalent width, the values of the latter should be taken as an order-of-magnitude estimate. The results of the fits to a variety of simulated spectra are summarized in Table 2.
4.1 Phase-averaged spectra

We start by considering the representative case of the phase-averaged spectra for model B2, simulated with $N_{H} = 10^{21}$ cm$^{-2}$. A pure BB fit gives an unacceptable $\chi^2_r$ and, more interestingly, it shows systematic residuals. The addition of a broad absorption line allows us to better fit the data, at least by partly removing systematic residuals. In Fig. 2, we show the unfolded spectrum with the residuals coming from the best-fitting BB+line model (removing the line for the sake of clarity), for a single realization of the synthetic spectrum.

The same qualitative behaviour is seen in all the cases in which the BB+line model fits better than the BB. The basic requirement needed to create a feature in the spectrum is that the fluxes from the coldest and hottest parts of the star be comparable. In these cases, the spectral distribution, to first order, consists of two Planckian shapes, whose temperatures and emitting areas represent an average value of the coldest and hottest parts. The spectral feature appears in the energy range between the two Planckian peaks. The larger the difference in temperature, the deeper the feature.

In Table 2, we have collected the fit results from several model temperatures (among the ones explored) for which the spectral feature appears. This sample is not meant to be a complete and systematic exploration of the large space of possible temperature distributions, but only an illustration of some of the tested cases. For each of them, we show the best-fitting parameters (with statistical errors) of the BB+line spectral model for a single realization, made with the indicated number of photons. In general, the central energy and the equivalent width are consistent with those observed in the considered sample.

In both the BB and the BB+line models, the inferred temperature $kT_{bb}$ corresponds to an average value of the redshifted surface temperatures (see also Perna et al. 2013). The values of $kT_{bb}$ for the BB and the BB+line models are compatible, while $R_{bb}$ can increase by up to ~10 per cent in the BB+line case, in order to account for the flux absorbed by the line. An important point is that, in all the cases, a 2BB fit (with absorption, if needed) fits well the simulated data, as long as the counts are less than a few $\times 10^3$ (depending on the model), in which case further small deviations can be resolved. In the models with $N_{H} = 0$, we find spurious lines for the cases in which the majority of the surface is almost invisible though still able to contribute to the low-energy spectrum, $E \lesssim 0.1$ keV. The same effect is obtained with hotter models but with large absorption, which again almost hides the cold component. In the case with absorption included, $N_{H}$ is left free to vary, and usually the best-fitting absorbed BB (or BB+line) value underestimates the absorption column by ~20–30 per cent with respect to the actual value used in the simulation. As a matter of fact, the single BB model tends to underestimate...
the flux coming from the colder part (which corresponds to a larger, colder region), thus needing less absorption to fit the data.

In Fig. 3, we show the correlation of $E_0/kT_{bb}$ with $N_H$ (left), and of $E_0$ with $kT_{bb}$ (right), both in real data (black) and in synthetic spectra (red). The spurious lines are centred at $E_0 \sim 4–9 \, kT_{bb}$, corresponding to the tail of energy larger than the Wien peak of the spectrum given by the best-fitting BB model. In observations, some of the lines lie in the same regions, while others are found at much larger energies, or much closer to the Wien peak. For those cases, this implies that the origin of the lines cannot be attributed to inhomogeneous surface temperatures.

Note also that selection effects limit the energy range in which lines can be found: solid claims cannot be made for $E_0$ close to the lower boundary of the energy domain. For large absorption, there are too few photons in the region of low energy (few hundreds of eV), and therefore no spectral details at low energy can be appreciated. The same applies to the upper region of Fig. 3 (left-hand panel): thermal photons in that part are too few for any deviation from a single BB to be statistically significant. Low values of $N_H \lesssim 10^{20} \, \text{cm}^{-2}$ slightly affect only the very low energy part of the spectrum, thus making $N_H$ poorly constrained and highly correlated with $kT_{bb}$ and $R_{bb}$ (see, for instance, two different fits for the model B4, with the same $N_{syn}^H = 10^{20} \, \text{cm}^{-2}$ in Table 2).

In general, A-like models need a few $\times 10^5$ photons to make the line detectable, while many of the B and C models need only 3–5 $\times 10^4$ photons: the stronger the anisotropy, the easier it is to observe deviations from a pure BB, unless absorption is very large (see some of the C models). Another difference lies in the inferred radius from the fit ($R_{bb}$): while for the A models $R_{bb}$ is only slightly smaller than the radius of the star (seen at infinity, $R^\infty = 13 \, \text{km}$), for the B and C models it is much smaller, corresponding to the size of the hotspot (see Fig. 1).

Last, we computed for each representative model, the predicted pulsed fraction (PF), defined as

$$PF = \frac{F_{\max}(\gamma) - F_{\min}(\gamma)}{F_{\max}(\gamma) + F_{\min}(\gamma)},$$

where $F_{\max}$ and $F_{\min}$ are, respectively, the maximum and minimum flux as a function of phase in a given energy band. We selected the 0.1–2 keV band, above which the thermal flux becomes negligible for most models. All the models are computed for an orthogonal rotator ($\psi = \xi = 90^\circ$), which yields the largest allowed value for the PFs for the considered emission model (BB). The observed PF of each source puts some constraints on the allowed range of angles, and this needs to be discussed case by case for specific objects. We will do so in the following section for the source RX J0806.4–4123.

4.1.1 An example: fit to J0806.4–4123

In the previous subsection, we have shown that the apparent lines in the simulated spectra have $E_0$ and $E_w$ values similar to the commonly observed ones. In the following, we directly test our models for a particular source, J0806.4–4123. To this aim, we processed the 33.6 ks-long XMM–Newton/EPIC-pn observation of 2003 April 24,
using SAS version 12, and employing the most updated calibration files.

In the left-hand panel of Fig. 4, we show the unfolded spectrum with the best-fitting BB+line model ($\chi^2 = 1.36$) with $kT_{\text{bb}} = 96$ eV, $E_0 = 486$ eV, $E_w = 30$ eV, and $N_H$ unconstrained. The line has been removed in the plot for clarity. Several different temperature distributions (either with one or two hot spots) are able to fit the spectrum better than the BB model and the BB+line model. An example of one of such cases is shown in the right-hand panel, with $N_H = (4.2 \pm 0.1) \times 10^{20}$ cm$^{-2}$, $\chi^2 = 1.18$. Two of the typical temperature profiles that fit the data (symmetric/asymmetric distributions) are shown in Fig. 5.

An independent, important constraint on the underlying temperature profile is provided by the pulsed profiles. For the XINSs, they are generally single-peaked, with relatively low PFs. In the particular case of the source J0806.4–4123, the PF in the EPIC-pn is 6 per cent in the 0.12–1.2 keV band (Haberl & Zavlin 2002). We hence explored the parameter space in the angles $\psi$, $\xi$ which can yield this modulation level, for both models. We note that, without the effect of interstellar absorption, the modulation level of the models in a wide energy band is low, even for an orthogonal rotator ($\psi = \xi = 90^\circ$). This is because, as already discussed, the models that yield spectral features are characterized by comparable fluxes in the hot and colder regions (dominant at opposite phases). However, for sources with high $N_H$, the colder component is largely absorbed, thus lowering the flux at the minimum of the pulsed profile and resulting in an increased PF in a wide band (see Perna, Heyl & Hernquist 2000, for an extensive discussion on this topic). This is particularly so for the single spot model.

Fig. 6 shows contour plots of the PF as a function of the angles $\psi$, $\xi$ for the two models used for the fit of J0806.4–4123 (Fig. 5). As expected, in each case, there is a range of viewing angles which yield values of the PF consistent with the observed value of 6 per cent (thick dashed line in the figure). In the single spot case, the profile is single peaked for all the choices along this degenerate region. On the other hand, for the double spot, some viewing geometries, even if consistent with the observed PF, can however be ruled out as they would yield a double-peaked profile, unlike that observed. Among the range of angles yielding PF $\sim 6$ per cent, we have selected, for the double spot, one particular choice of angles yielding a double-peaked profile, and another yielding a single peaked one (favoured by the observations). The single peak profiles require solutions to be close to the main diagonal, with allowed angles in the range $\psi, \xi \approx 10^\circ$–$30^\circ$. On the other hand, solutions such as the one

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3 Note that Kaplan & van Kerkwijk (2009b) further improve the fit by considering a model with a BB and two absorption lines.
displayed with $\xi \approx 85^\circ$ and $\psi \approx 60^\circ$ would show a second (lower) maximum in the pulsed profile.

Finally, we should note that the derived values of the viewing angles should be taken with caution, for two reasons: first, here we have assumed BB, perfectly isotropic emission, and realistic atmospheres are known not to be such (e.g. Zavlin, Pavlov & Shibanov 1996), secondly, a change of viewing angles implies, in turn, slightly different phase-average spectra, and a non-trivial, iterative fine tuning of both temperature distribution and viewing angles would be needed to achieve a fully consistent fit of all observed properties.

4.2 Phase-resolved analysis

The phase-resolved spectra strongly depend on the inclination and viewing angles. In axial symmetry, the most extreme phase-variability (and PF) is obtained when $\xi = \psi = 90^\circ$ (orthogonal rotator). The smaller the angles, the less distinguishable in phase are the hot and cold regions, because all the hot spots/rings are seen in most phases.

We analysed the fake phase-resolved spectra for model B2 with $\xi = \psi = 90^\circ$, considering 20 different phase angles $\gamma$. Again, we fit with a BB model, with or without a Gaussian absorption line with $\sigma$ fixed at 150 eV.

In Fig. 7, we plot $\chi^2_\nu$ and the value of $E_w$ as a function of density. The BB+line model fits significantly better than the BB for all the phases at which the northern hotspot is seen. On the other hand, around $\gamma = \pi$, the hotspot is not seen, the temperature distribution is more homogeneous, and a single BB fits well. The equivalent width remains constant in phase, until the hotspot goes out of sight, and $E_w$ approaches zero. When the spurious line is detected, its centroid, $E_0$, remains almost constant, within errors. On the other hand, models of family A show very little variability, because, being axisymmetric, at least one of the two hot poles is always seen.

Therefore, asymmetric temperature distributions are characterized by a strong phase variability in the equivalent width of the spurious line, while the line centroid is barely affected. While these phase-dependent properties may not be unique to spectral features due to temperature inhomogeneities, they should be kept in mind in the process of interpreting the origin of spectral features, case by case.

5 DISCUSSION

We have computed synthetic X-ray spectra of NSs for several inhomogeneous surface temperature maps and found that, in some cases, the spectra present features compatible with broad absorption lines at a high-significance level. The distinguishing characteristic of the temperature distributions leading to these spectral distortions is one or more hot, small regions with a temperature larger by at least a factor of about 1.5–2 than the average temperature of the rest of the surface. The hotspot(s) and the cold parts should give similar contribution to the flux; the poor sensitivity of the instruments at low energy and/or the interstellar absorption, partially hide the Planckian emission produced by the coldest regions. As a consequence, the spurious line appears between the two Planckian peaks. In light of our analysis, we propose that the need for absorption lines in the fits to some isolated NSs may be a hint for inhomogeneous temperature distributions, but the opposite is not generally true: an inhomogeneous temperature does not always imply the appearance of a spectral line. The NS in the SNR Kes79 (Halpern & Gotthelf 2010) shows strong hints for anisotropy (two BBs in the spectral fits, and/or a large PF), but it does not require a line in the spectrum.
In our synthetic models, the values of the line-model parameters ($E_0$ and $E_w$) are in the same ranges as the observed ones. The spurious lines always appear beyond the Wien peak of the BB+line model, and $E_w \sim 4-9 \text{ kT}_{bb}$. Most objects (e.g. XINSs and PSRs), show a similar position of $E_0$. However, conclusions cannot be drawn only on the basis of this property; rather, each object should be considered separately. As an example, we have performed a fit to RX J0806.4–4123, finding several different temperature distributions able to give acceptable fits, better than the BB+line fit. This shows that, at least for this object, a temperature inhomogeneity can produce deviations from a pure BB model similar to the observed ones. The gross features of, on the other hand, other sources like CCO 1E1207.4–5209 and the XINSs RX J1308.6+2127 are cases for which the deviations from a BB spectrum do not appear to be reproducible by inhomogeneous temperature distributions. The exceptional spectral complexity of these sources cannot be mimicked, even qualitatively, by any of the many surface temperatures that we have tested.

In general, we remark that, given the wide space of parameters of the temperature modelling, reconstructing the surface temperature map is a highly degenerate problem. Moreover, for the purpose of isolating spectral effects due to temperature anisotropy alone, here we have used local BB emission rather than realistic, magnetized atmospheric/condensed surface models. These are the reasons for which we did not attempt individual fits to all the sources. Rather, we have demonstrated that the contribution to spectral features from temperature inhomogeneity can be significant, and hence this should be accounted for in combination with more sophisticated emission models.

To conclude, we note that, while current observations still allow several interpretations for the observed absorption features, the very large effective area of the planned X-ray mission Athena+ (Nandra et al. 2013) will provide top-quality spectra, with the possibility of fine-tuning the spectral models and possibly discriminating between different underlying physical mechanisms.

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**REFERENCES**
Albano A., Turolla R., Israel G. L., Nobili L., Stella L., 2010, ApJ, 722, 788
Arnaud K. A., 1996, in Jacoby G. H., Barnes J., eds, ASP Conf. Ser. Vol. 101, Astronomical Data Analysis Software and Systems V. Astron. Soc. Pac., San Francisco, p. 17
Becker W., 2009, in Becker W., ed., Astrophysics and Space Science Library, Vol. 357, Neutron Stars and Pulsars. Springer-Verlag, Berlin, p. 91
Beloborodov A. M., 2013, ApJ, 777, 114
Bernardini F. et al., 2009, A&A, 498, 195
Bernardini F., Perna R., Gotthelf E. V., Israel G. L., Rea N., Stella L., 2011, MNRAS, 418, 638
Bignami G. F., Caraveo P. A., De Luca A., Mereghetti S., 2003, Nature, 423, 725
Burwitz V., Haberl F., Neuhaeuser R., Predelh P., Trumper J., Zavlin V. E., 2003, A&A, 399, 1109
Chen H.-H., Ruderman M. A., Sutherland P. G., 1974, ApJ, 191, 473
Cheng A. F., Ruderman M. A., 1980, ApJ, 235, 576
De Luca A., Mereghetti S., Caraveo P. A., Moroni M., Mignani R. P., Bignami G. F., 2004, A&A, 418, 625
De Luca A., Caraveo P. A., Mereghetti S., Negroni M., Bignami G. F., 2005, ApJ, 623, 1051
de Luca A. et al., 2012, MNRAS, 421, L72
de Vries C. P., Vink J., Mendez M., Verbunt F., 2004, A&A, 415, L31
Gotthelf E. V., Perna R., Halpern J. P., 2010, ApJ, 724, 1316
Gotthelf E. V., Halpern J. P., Alford J., 2013, ApJ, 765, 58
Haberl F., Zavlin V. E., 2002, A&A, 391, 571
Haberl F., Schwope A. D., Hambaryan V., Hasinger G., Motch C., 2003, A&A, 403, L19
Haberl F., Zavlin V. E., Trümper J., Burwitz V., 2004a, A&A, 419, 1077
Haberl F. et al., 2004b, A&A, 424, 635
Haberl F., Turolla R., de Vries C. P., Zane S., Vink J., Mendez M., Verbunt F., 2006, A&A, 451, L17
Halpern J. P., Gotthelf E. V., 2005, ApJ, 618, 874
Halpern J. P., Gotthelf E. V., 2010, ApJ, 709, 436
Halpern J. P., Ruderman M., 1993, ApJ, 415, 286
Hambaryan V., Suleimanov V., Schwoepe A. D., Neuhaeuser R., Werner K., Potekhin A. Y., 2011, A&A, 534, A74
Ho W. C. G., 2007, MNRAS, 380, 71
Ho W. C. G., Lai D., 2001, MNRAS, 327, 1081

**Figure 7.** Phase-resolved spectra, for the model B2, without absorption. Left: $\chi^2/\nu$ of the best-fitting BB (dashed) or BB+line model (solid) as a function of phase. Right: equivalent width, $E_w$, as a function of phase.
Ho W. C. G., Lai D., 2003a, in Hubeny I., Mihalas D., Werner K., eds, ASP Conf. Ser. Vol. 288, Stellar Atmosphere Modeling. Astron. Soc. Pac., San Francisco, p. 621
Ho W. C. G., Lai D., 2003b, MNRAS, 338, 233
Ho W. C. G., Lai D., Potekhin A. Y., Chabrier G., 2003, ApJ, 599, 1293
Ho W. C. G., Kaplan D. L., Chang P., van Adelsberg M., Potekhin A. Y., 2007, MNRAS, 375, 821
Hohle M. M., Haberl F., Vink J., de Vries C. P., Neuhauser R., 2012a, MNRAS, 419, 1525
Hohle M. M., Haberl F., Vink J., de Vries C. P., Turolla R., Zane S., Méndez M., 2012b, MNRAS, 423, 1194
Ibrahim A. I., Swank J. H., Parke W., 2003, ApJ, 584, L17
Kaplan D. L., van Kerkwijk M. H., 2009a, ApJ, 692, L62
Kaplan D. L., van Kerkwijk M. H., 2009b, ApJ, 705, 798
Kaplan D. L., van Kerkwijk M. H., 2011, ApJ, 740, L30
Kargaltsev O., Durant M., Misanovic Z., Pavlov G. G., 2012, Science, 337, 946
McLaughlin M. A. et al., 2007, ApJ, 670, 1307
Mereghetti S., 2008, A&AR, 15, 225
Miller M. C., 1992, MNRAS, 255, 129
Miller J. J., McLaughlin M. A., Rea N., Lazaridis K., Keane E. F., Kramer M., Lyne A., 2013, ApJ, 766, 104
Mori K., Hailey C. J., 2006, ApJ, 648, 1139
Mori K., Chonko J. C., Hailey C. J., 2005, ApJ, 631, 1082
Nandra K. et al., 2013, preprint (arXiv:1306.2307)
Özel F., 2001, ApJ, 563, 276
Page D., 1995, ApJ, 442, 273
Page D., Geppert U., Kuiper M., 2007, Ap&SS, 308, 403
Pavlov G. G., Shibanov Y. A., Zavlin V. E., Meyer R. D., 1995, in Alpar M. A., Kiziloglu U., van Paradijs J., eds, The Lives of the Neutron Stars. Kluwer, Dordrecht, p. 71
Pérez-Azorín J. F., Pons J. A., Miralles J. A., Miniutti G., 2006, A&A, 459, 175
Perna R., Gotthelf E. V., 2008, ApJ, 681, 522
Perna R., Heyl J., Hernquist L., 2000, ApJ, 538, L159
Perna R., Viganò D., Pons J. A., Rea N., 2013, MNRAS, 434, 2362
Pieres A. M., Motch C., Turolla R., Schwope A., Pilia M., Treves A., Popov S. B., Janot-Pacheco E., 2012, A&A, 544, A17
Pieres A. M., Haberl F., Zavlin V. E., Motch C., Zane S., Hohle M. M., 2014, A&A, 563, A50
Pons J. A., Walter F. M., Lattimer J. M., Prakash M., Neuhauser R., An P., 2002, ApJ, 564, 981
Pons J. A., Miralles J. A., Geppert U., 2009, A&A, 496, 207
Rea N., Israel G. L., Stella L., Oosterbroek T., Mereghetti S., Angelini L., Campana S., Covino S., 2003, ApJ, 586, L65
Rea N., Oosterbroek T., Zane S., Turolla R., Méndez M., Israel G. L., Stella L., Haberl F., 2005, MNRAS, 361, 710
Rea N., Zane S., Turolla R., Lyutikov M., Götz D., 2008, ApJ, 686, 1245
Romani R. W., 1987, ApJ, 313, 718
Sanwal D., Pavlov G. G., Zavlin V. E., Teter M. A., 2002, ApJ, 574, L61
Sartore N., Tiengo A., Mereghetti S., De Luca A., Turolla R., Haberl F., 2012, A&A, 541, A66
Schwope A. D., Hambaryan V., Haberl F., Motch C., 2007, Ap&SS, 308, 619
Suleimanov V., Potekhin A. Y., Werner K., 2009, A&A, 500, 891
Suleimanov V. F., Pavlov G. G., Werner K., 2010, ApJ, 714, 630
Suleimanov V. F., Pavlov G. G., Werner K., 2012, ApJ, 751, 15
Tiengo A. et al., 2013, Nature, 500, 312
Turolla R., 2009, in Becker W., ed., Astrophysics and Space Science Library Vol. 357, Neutron Stars and Pulsars. Springer-Verlag, Berlin, p. 141
van Adelsberg M., Lai D., 2006, MNRAS, 373, 1495
van Adelsberg M., Lai D., Potekhin A. Y., Arras P., 2005, ApJ, 628, 902
van Kerkwijk M. H., Kaplan D. L., Durant M., Kulkami S. R., Paerels F., 2004, ApJ, 608, 432
van Riper K. A., 1988, ApJ, 329, 339
Viganò D., Rea N., Pons J. A., Perna R., Aguilar D. N., Miralles J. A., 2013, MNRAS, 434, 123
Zane S., Cropper M., Turolla R., Zampieri L., Chiuregato M., Drake J. J., Treves A., 2005, ApJ, 627, 397
Zavlin V. E., Pavlov G. G., 2004, ApJ, 616, 452
Zavlin V. E., Pavlov G. G., Shibanov Y. A., 1996, A&A, 315, 141
Zavlin V. E., Pavlov G. G., Trumper J., 1998, A&A, 331, 821

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