Velocity selected production of $^2S$ metastable positronium

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Positronium in the $^2S$ metastable state exhibits a low electrical polarizability and a long lifetime (1140 ns) making it a promising candidate for interferometry experiments with a neutral matter-antimatter system. In the present work, $^2S$ positronium is produced - in absence of electric field - via spontaneous radiative decay from the $^3P$ level populated with a 205 nm UV laser pulse. Thanks to the short temporal length of the pulse, 1.5 ns full-width at half maximum, different velocity populations of a positronium cloud emitted from a nanochanneled positron/positronium converter were selected by delaying the excitation pulse with respect to the production instant. $^2S$ positronium atoms with velocity tuned between $7 \times 10^3$ m/s and $10 \times 10^3$ m/s were thus produced. Depending on the selected velocity, a $^2S$ production efficiency ranging from $\sim 0.8\%$ to $\sim 1.7\%$, with respect to the total amount of emitted positronium, was obtained. The observed results give a branching ratio for the $^3P \rightarrow ^2S$ spontaneous decay of $(9.7 \pm 2.7)\%$. The present velocity selection technique could allow to produce an almost monochromatic beam of $\sim 1 \times 10^3$ $^2S$ atoms with a velocity spread $< 10^4$ m/s and an angular divergence of $\sim 50$ mrad.

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Positronium (Ps) is one of the few matter/antimatter systems (with antihydrogen and muonium) being considered for probing experimentally the gravitational interaction. Several experimental schemes based on long-lived Ps beams have been proposed, either letting the atoms free-fall in a drift tube or by using a mater-
wave atom interferometer \[8\] to measure their vertical displacement with a position-sensitive detector. Gravity (or any other force acting on the atoms) can then be worked out if the average velocity of the atoms is known \[3, 8\].

All the suggested schemes involve laser excitation to long-lived excited states to overcome the lifetime limitation of the \(1^3\)S ground state (142 ns) where Ps is normally produced. An effective and widely adopted choice consists in laser-exciting the atoms to the Rydberg levels, where lifetimes spanning from tens of ms up to several ms can be obtained \[9, 10\]. Atoms in Rydberg states are, in general, sensitive to electric field gradients \[11\] which can modify their trajectories. This is due to their large electrical polarizability (up to \(\sim 10^{-32} \text{ C m}^2 \text{ V}^{-1}\) for Ps in \(n = 15\) \[12, 13\]). Ps Rydberg sublevels with large electrical dipole can be guided and focused \[12, 13\] while the selective excitation to sublevels with low dipole moment has been proposed \[14\] as a method to minimize the deflection of Rydberg Ps in interferometric measurements with physical gratings \[15\].

An alternative way to produce a beam of long-lived Ps with lower electrical polarizability (\(\sim 10^{-38} \text{ C m}^2 \text{ V}^{-1}\)) consists in laser exciting the atoms to their \(2^3\)S metastable level \[15\], whose lifetime is 1.14 \(\mu\)s in vacuum and in the absence of electric field \[16\]. A beam of \(2^3\)S Ps atoms (of known average velocity) has been shown to be suitable for improving the inertial sensitivity in proposed matter-wave interferometric layouts \[8\]. Moreover, the availability of \(2^3\)S Ps with average velocity < \(10^5 \text{ m s}^{-1}\) would allow keeping the interferometer compact in length (\(L \lesssim 1 \text{ m}\)), thus easing the control of thermal and vibrational noise \[17\].

Producing fast \(2^3\)S Ps with energies of several eV has already been demonstrated via \(e^+\) collisions with solid \[18, 20\] or gaseous targets \[21, 22\]. \(2^3\)S Ps atoms with a beam Maxwellian distribution at around 600 K (average speed > \(1.4 \cdot 10^5 \text{ m s}^{-1}\)) were also produced via Doppler-free two photon excitation of ground-state atoms of Ps desorbed from metallic surfaces \[23\, 25\] and \(1^3\)S–\(2^3\)S two photon excitation of Ps emitted from porous silicon \[26\]. Production of \(2^3\)S Ps via single photon excitation of ground-state atoms to mixed \(2^3\)S–\(2^1\)P in electric fields \[15\] and the single photon excitation of ground-state atoms to \(3^1\)P levels with subsequent radiative decay to \(2^3\)S \[16\] have been recently demonstrated. The reduction of the \(2^3\)S lifetime in electric fields due to Stark mixing has also been studied \[16\].

In the present work we investigate the feasibility of a source of metastable \(2^3\)S Ps with defined and tunable velocity in the absence of electric field. The \(2^3\)S level is populated by spontaneous radiative decay of laser-excited \(3^1\)P Ps atoms. The tuning of the \(2^3\)S Ps velocity is achieved by varying the delay of the \(1^3\)S–\(3^1\)P excitation pulse between 20 ns and 65 ns from the \(e^+\) implantation time in a nanochannelled silicon \(e^+\)–Ps converter \[27\], thus selecting Ps populations emitted after different permanence times in the target \[28, 29\] and consequently with different velocities \[30, 31\].

In our experiment, Ps is formed when \(\sim 7 \text{ ns bursts of } \sim 10^7 \text{ e}^+\), prepared in the AE\(\bar{g}\)IS \(e^+\) system (see \[16\] for a detailed description of the apparatus) are electro-magnetically transported and implanted at 3.3 keV into a Si (111) p-type crystal where nanochannels were previously produced via electrochemical etching and thermal oxidized in air \[16\]. Ps produced inside the converter out-diffuses into vacuum through the nanochannels losing a fraction of its emission energy by collision with the walls. The Si target was kept at room temperature and \(e^+\) were implanted into it with a spot of \(\sim 3 \text{ mm in size}\). Measurements previously performed on identical \(e^+\)–Ps converters indicated a wide angular emission of Ps from the nanochannels \[16, 33\]. A schematic of the experimental chamber is illustrated in Fig. 1.

![Figure 1: Schematic of the experimental chamber with example Monte Carlo in-flight and collision annihilation distributions for an \(1^3\)S Ps population (light and dark red dots) and for a \(2^3\)S Ps population (yellow and blue dots). The line-shaped annihilations’ distribution of \(2^3\)S atoms is due to the UV laser Doppler selection.](image_url)

In the target region, \(e^+\) are guided by a 25 mT magnetic field and focused by an electrostatic lens formed by the last electrode of the transfer line set at \(-3000 \text{ V}\) and the target kept at ground potential (see Fig. 1 for the geometry), inducing an electric field of about 300 V cm\(^{-1}\) in front of the converter. Since this electric field shortens considerably the \(2^3\)S lifetime \[13, 16\], for the present measurements the focusing electrode was switched off \(\sim 5 \text{ ns}\) after the \(e^+\) implantation using a fast switch with a rise time of \(\sim 15 \text{ ns}\) (from \(-3000 \text{ V}\) to 0 V).
Ps emitted into vacuum was subsequently excited from the 1S ground state to 3P sublevel manifold with an UV laser pulse set at the transition resonance wavelength $\lambda_{UV} = (205.045 \pm 0.005)$ nm. The laser setup is described in detail elsewhere [33]. The UV pulse energy was kept above 60 mJ and the effective size of the spot was about 3.0–3.5 mm full width at half maximum (FWHM) both in horizontal and vertical direction in front of the target. The laser beam was aligned grazing the target and its position and size were monitored with a CCD camera on a 1-in. MACOR screen placed inside the vacuum region (a few cm away from the target). The UV pulse had a horizontal polarization (i.e. perpendicular to the target), a nearly Gaussian temporal profile with a FWHM of 1.5 ns, and a Gaussian-like spectral profile with a bandwidth $\sigma_{UV} = 2\pi \times 120$ GHz.

The laser bandwidth is narrower than the Doppler profile of Ps emitted from the used $e^+–Ps$ converter ($\sim 2\pi \times 470$ GHz, see [33]). As a consequence, the UV pulse selectively excites to 3P only the fraction of the emitted atoms with a velocity component parallel to the laser propagation axis, $v_\parallel$, with $|v_\parallel| < 2.5 \times 10^4$ m s$^{-1}$. Following the excitation, a fraction of Ps in the 3P sublevel spontaneously decays to 2S emitting a 1312 nm photon with an expected branching ratio of 10 % in the presence of a 25 mT magnetic field [16]. The atoms in the 2P sublevel retain - with a good approximation - the original velocity distribution, since both recoil velocities for the absorption of a 205 nm photon ($\approx 1.8 \times 10^3$ m s$^{-1}$) and the emission of a 1312 nm photon ($\approx 2.8 \times 10^2$ m s$^{-1}$) are negligible. The UV pulse was delayed, with respect to the $e^+$ implantation time, from 20 ns (to let the electric field reach 0 V cm$^{-1}$) up to 65 ns by using a SRS DG645 digital delay generator.

The time distribution of gamma rays emitted by $e^+$ and Ps annihilations, i.e. the so-called Single-Shot Positron Annihilation Lifetime Spectroscopy (SSPALS) spectrum, was acquired with the same procedure used in [16, 33]. A 20 × 25 × 25-mm PbWO$_4$ scintillator, coupled to a Hamamatsu R1265-100 photomultiplier tube (PMT) and digitized by a HD4096 Teledyne LeCroy oscilloscope, was placed 40 mm above the target (Fig. 1). In the presence of Ps formation, SSPALS spectra present a prompt peak, given by the fast $2\gamma$ annihilations of e$^+$ implanted in the target, and a tail that is dominated by the 3$\gamma$ decay of Ps emitted into vacuum (Fig. 2). The changes in the Ps population induced by the interaction with laser light affect the area under the tail. This effect can be quantified by using the $S$ parameter evaluated as:

$$S = \frac{A_{off} - A_{on}}{A_{off}},$$

where $A_{off}$ and $A_{on}$ are the averages of the normalized areas $A_{off}^i$ and $A_{on}^i$ below the $i$-th SSPALS shot, calculated in a given time window with lasers off and on respectively [33]. The areas were normalized by using the detrending procedure described in [16], which mitigates the effect of eventual slow drifts in the positron beam intensity. The fraction of Ps excited to 3P with the UV pulse was evaluated by selectively photoionizing the excited atoms with an IR pulse ($\lambda_{IR} = 1064$ nm, energy of 50 mJ and temporal FWHM of 4 ns [33]). The 1S–3P photoionization process results in a decrease of the Ps population decaying into $3\gamma$ at late times.

Samples of 200 single SSPALS shots alternating UV+IR lasers on and off were collected with different laser delays to measure the 1S–3P excitation efficiency. A $S = (13.8 \pm 2.2)$ % was observed in the selected 50–500 ns time window after the prompt peak for a laser delay of 20 ns, in agreement with the results of Ref. [16, 33]. Repeating the measurement delaying the UV+IR laser pulses to 35 ns and 50 ns, the $S$ signal decreased by ~30 %, to $S = (8.8 \pm 2.6)$ %, and by ~60 %, to $S = (6.8 \pm 2.9)$ %, respectively, since an increasing fraction of Ps atoms already left the target proximity before the laser pulse.

Sending the UV laser only, a fraction of the excited Ps is allowed to spontaneously decay from 3P to 2S. In absence of an electric field, as in the present case, the lifetime of Ps in the 2S state is eight times longer than in the 1S state (1140 ns vs 142 ns) [2, 16]. Due to this longer lifetime, a larger fraction of atoms survives in-flight annihilation and reaches the experimental chamber walls, where it annihilates in 2$\gamma$ with an electron of the medium producing a signal excess clearly identifiable in SSPALS spectra (Fig. 2).

A previously developed Monte Carlo (MC) code [2, 16] was used to calculate the expected spatial and the temporal distributions of 1S and 2S annihilations in the geometry of our experimental chamber. This code calculates the atoms flight trajectories and position and time annihilation distributions, accounting for both in-flight self-annihilations and collisions with the walls, by integrating the equation of motion for the single particles and the optical rate equations of the internal level dynamics, while testing for collisions with the chamber walls. The final annihilation distributions are obtained upon averaging over the sample of atoms sorted on the initial velocity and position distributions. The free parameters are the 1S–3P excitation efficiency (obtained experimentally from the UV+IR data), the 3P–1S quenching efficiency (assumed to be 17% in our 25 mT magnetic field [16, 33]), the 3P–2S branching efficiency (to be determined), plus those specifying the initial position/velocity distributions. As no external electric field is present and the expected maximum motional Stark electric field is $\approx 25$ V cm$^{-1}$ in our 25 mT magnetic field with a Ps velocity of the order of $\approx 10^3$ m s$^{-1}$ (corresponding to an optical decay rate of 2S in electric field of $\approx 100$ kHz [16]), the optical decay of 2S atoms was not included in the simulations. Ultimately the code produces a model...
Figure 2: Average of 200 SSPALS spectra of Ps in vacuum with UV laser off (blue) and on (red), normalized to the peak height. The potential on the focusing electrode is also shown (dashed line). The arrow marks the laser pulse instant (here 20 ns after the peak) and the vertical lines delimit the area used to conduct the detrending analysis of the $S$ parameter shown in the inset (see text and [16]). Full circles and empty squares are the detrended areas with/without laser (i.e. $A_{on}$ and $A_{off}$). The sideways Gaussian curves are the distributions of $A_{on}$ (red) and $A_{off}$ (blue).

estimate of the $S$ parameter that can be directly compared with experimental data.

In order to give a pictorial representation of the expected annihilation positions of the $1^3S$ and $2^3S$ populations, a MC simulation has been conducted with $10^4$ Ps atoms in each population (i.e. not reflecting the real $2^3S/1^3S$ relative abundance to emphasize the rare annihilations of the $1^3S$ fraction on the walls) and setting an uniform velocity of $10^5 \text{ m s}^{-1}$ in modulus for all Ps atoms (Fig. 1). Isotropic emission of $1^3S$ Ps from the converter and the Doppler selection from a $2\pi \times 120 \text{ GHz}$ excitation laser were assumed [31, 36]. According to the MC simulations, around 60% of the produced $2^3S$ Ps reaches the walls as opposed to only $\sim 1\%$ of $1^3S$ atoms with the same velocity. This causes the additional annihilations in the tail of the SSPALS spectra shown in Fig. 2 leading to negative values of the $S$ parameter (Eq. 1).

Experimentally, when the UV laser delay is set to 20 ns, the excess of annihilations due to $2^3S$ atoms reaching the chamber walls is observed between 500 ns and 800 ns from the peak maximum, giving a $S = (−10.2 \pm 3.4)\%$ (Fig. 2 inset). The time when this excess appears can be controlled by varying the laser pulse delay.

Indeed, nanochanneled Si $e^+–$Ps converters emit Ps in a broad distribution of velocities [30, 31]. Emission velocity is mostly dependent on the time needed to escape from the nanochannels into vacuum (or permanence time

28, 29): the highest values correspond to the shortest Ps permanence times (1 ns or less) and the lowest ones to the longest permanence times (up to 20 ns) [29, 31]. As a matter of fact, the fraction that resides longer in the nanochannels loses more energy by collision with the walls. The UV laser pulse, thanks to its brief duration and its limited spatial dimension, excites only the fraction of the emitted Ps in front of the target at the time when the laser is shot. Ps atoms with different permanence times and consequently different velocities can be thus selected varying the laser timing.

Measurements as in Fig. 2 were repeated by retarding the UV laser shot to 35, 50 and 65 ns. The $−S$ parameter was calculated using time windows of 300 ns in steps of 50 ns. The continuous lines are the Monte Carlo best fits (see text) of the $−S$ parameter. The weak signal at 65 ns does not allow to perform a reliable fit.

Figure 3: $−S$ parameter as a function of the time elapsed from the prompt peak for different UV laser delays (20, 35, 50 and 65 ns). The $−S$ parameter was calculated using time windows of 300 ns in steps of 50 ns. The continuous lines are the Monte Carlo best fits (see text) of the $−S$ parameter. The weak signal at 65 ns does not allow to perform a reliable fit.
annihilations almost disappeared with 65 ns, indicating that the largest part of the Ps emitted by the converter has already left the laser spot. A rough estimation of the average velocity (for each delay setting) is promptly obtained considering the average distance between the converter and the front wall (6 cm, see Fig. 1): 6 cm/650 ns ≃ 9.2 × 10^4 m s⁻¹, 6 cm/800 ns ≃ 8.0 × 10^4 m s⁻¹ and 6 cm/900 ns ≃ 7.0 × 10^4 m s⁻¹ for UV pulse delays of 20 ns, 35 ns and 50 ns respectively.

A more accurate estimation of the 2S velocity distribution was obtained by fitting the experimental -S versus time curves (Fig. 3) with the previously introduced MC model, assuming the initial 2S Ps atoms velocities to be distributed as a 1D-Gaussian function in modulus and uniformly in angle. The initial position distribution was assumed point-like as the e⁺ spot radius ~ 1.5 mm is much smaller than other distances at play.

The superimposed solid lines in Fig. 3 were obtained from the MC varying the 3P–2S efficiency and the average velocity in order to find the best agreement between data and predictions. The best-fit parameters and their statistical errors are summarized in Tab. I. The MC model fit agrees with the previous rough estimation of the average 2S velocity for each delay setting. Moreover, it constraints the standard deviation of each 2S velocity distribution to Δv < 1 · 10^4 m s⁻¹ in all the three cases, pointing out that this source of 2S is roughly monochromatic to Δv/v ≲ 14% or better (the limit of our current sensitivity). A branching efficiency for the 3P–2S transition of around 10%, in agreement with the expected theoretical value [10], was also found (Tab. I). Note that found values and error bars may be affected by unaccounted systematical uncertainties due the approximated time, position and velocity distributions of emitted Ps and laser excitation dynamics. However the results were verified not to be changing significantly (i.e. by more than 1.0 · 10^4 m s⁻¹) using other reasonable Ps emission models, for instance uniform velocity and non-uniform angular emission with an angle-cut at 60° or higher [31, 30].

In conclusion, we have demonstrated the possibility to produce 2S Ps via 3P excitation and spontaneous decay with a selected average velocity in the range 7 - 10 · 10^4 m s⁻¹ and with Δv < 1 · 10^4 m s⁻¹ (< 14% monochromaticity) in the absence of electric field. With present positron-Ps converters [11, 92] and bursts of 10^7 e⁺ [37, 58], 3 · 8 · 10^4 Ps atoms every minute in 2S level can be obtained (according to the selected velocity range). Since the UV laser also acts as angular selector due to its limited bandwidth, these 2S Ps atoms expand in the space as depicted in Fig. 1. Using a proper iris, every minute an almost monochromatic pulsed beam of ≃ 1 · 10^3 2S atoms with an angular divergence of 50 mrad could be obtained. An enhancement of the beam intensity, while retaining the observed velocity selection, could be envisaged using stimulated emission, i.e. increasing the 3P–2S transition rate and its branching efficiency. Further reduction of the 2S Ps atoms velocity looks also feasible thanks to the observed thermal Ps emitted by similar e⁺–Ps converters when held at cryogenic temperatures [30]. Selecting this thermal fraction should allow to produce monochromatic 2S with velocity in the range of low 10^4 m s⁻¹. The development of long-lived 2S Ps beams - with defined and tunable velocity - could open the possibility to perform interferometry measurements with Ps [8].

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| Laser delay | 1S → 3P efficiency | 3P → 2S efficiency | 2S average velocity |
|-------------|---------------------|---------------------|---------------------|
| 20 ns       | (13.8 ± 2.2) %      | (9.7 ± 2.7) %       | (1.0 ± 0.1) · 10^7 m s⁻¹ |
| 35 ns       | (8.8 ± 2.6) %       | (8.7 ± 5.0) %       | (0.8 ± 0.1) · 10^7 m s⁻¹ |
| 50 ns       | (6.8 ± 2.9) %       | (10.1 ± 6.2) %      | (0.7 ± 0.1) · 10^7 m s⁻¹ |

Table I: Comparison of the experimental 1S–3P efficiency (from photoionization) and the best found parameters with the Monte Carlo model for different laser delays.
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