Paramagnetic effect in YBa$_2$Cu$_3$O$_{7-x}$ grain boundary junctions.

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A detailed investigation of the magnetic response of YBa$_2$Cu$_3$O$_x$ grain boundary Josephson junctions has been carried out using both radio-frequency measurements and Scanning SQUID Microscopy. In a nominally zero-field-cooled regime we observed a paramagnetic response at low external fields for 45° asymmetric grain boundaries. We argue that the observed phenomenology results from the d-wave order parameter symmetry and depends on Andreev bound states.

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Superconductors below the transition temperature $T_c$ usually expel an external magnetic field. This phenomenon, known as the Meissner effect, leads to diamagnetism. It was therefore quite unexpected that a paramagnetic Meissner effect (PME) was observed in a field cooled regime for ceramic Bi$_2$Sr$_2$CaCu$_2$O$_{8-δ}$ (BISCOO). For an explanation, it was proposed that below $T_c$, there are randomly distributed spontaneous orbital currents in the sample. These currents can be oriented by an external magnetic field, providing a paramagnetic signal. Sigrist and Rice pointed out that the spontaneous orbital currents can be caused by a $d_{x^2-y^2}$-wave symmetry of the superconducting state. Indeed, the d-wave scenario predicts the existence of Josephson junctions in which the Josephson energy reaches a minimum for a phase difference across the junction at $\phi = \pi$ ($\pi$-contact). In ceramic high-$T_c$ superconductors (HTS) the grains can form loops which contain odd numbers of $\pi$-contacts, so called frustrated loops. In such a system the energy is minimized by a configuration with a spontaneous current flowing in the loop. In particular, for a $\pi$-contact with a “conventional” current-phase relationship $I = I_c \sin(\phi + \pi)$ inserted in a loop, the gain in Josephson energy exceeds the loss of magnetic energy when the parameter $\beta$ satisfies $\beta = 2\pi LI_c/\Phi_0 > 1$, where $\Phi_0$ is the flux quantum, $I_c$ is the critical current and $L$ is a loop inductance. However, a paramagnetic signal in the field-cooled regime has also been observed for conventional superconductors.

In order to distinguish between different origins of paramagnetism Rice and Sigrist proposed to detect spontaneous orbital currents by a SQUID microscope for zero-field cooled samples. In a granular BISCOO sample exhibiting a paramagnetic signal, spontaneous magnetization has indeed been observed. The PME and the presence of spontaneous currents therefore represent two of the main features induced by the d-wave order parameter symmetry in HTS.

A study of these phenomena on a more controlled system, such as a grain boundary (GB) line, could shed additional light on the relation between these effects and their influence on the properties of the grain boundary Josephson junctions (GBJJ).

In this paper, for the first time, we give evidence of a paramagnetic behavior for zero-field cooled asymmetric 45° YBa$_2$Cu$_3$O$_x$ (YBCO) GBJJ. The paramagnetic signal, that has been previously observed in two-dimensional systems, has been in this case detected in a single GB line and related to basic mechanisms in HTS JJs. Apart from conventional transport properties and Scanning SQUID Microscopy (SSM) measurements, we exploited radio-frequency measurements, which are very sensitive and provide a direct test for paramagnetic signals as demonstrated below. This is a further manifestation of the d-wave nature of the order parameter, but it is also relevant for the understanding of transport across GBJJs and in particular on the incidence of Andreev bound states.

The idea of the rf measurements is the following. The sample of interest is inductively coupled to a high-quality (quality factor $Q \approx 300$) parallel resonant circuit of inductance $L_T$, capacitance $C_T$. Experimentally this is realized by flip chip configuration - the sample is placed on the top of a small solenoid coil perpendicular to its axis. For such an arrangement, the effective impedance of the tank circuit coupled to the sample is a function of the external magnetic field $H_e$ applied to the sample. This field consists of a dc and an rf component as induced by a current $I_{dc}$ (in fact of very low frequency) and an rf oscillating current $I_{rf}$ in the tank coil, hence $H_e = H_{dc} + H_{rf}$. In order to avoid the nucleation of rf “vortices” and other nonlinear effects, the amplitude of $H_{rf}$ is small, so that $H_{rf} \ll H_{c1}, H_{dc}$, where $H_{c1}$ is the first critical field, therefore $H_e \approx H_{dc}$. If $L_{eff}(H_{dc})$ and $R_{eff}(H_{dc})$ are the effective inductance and the effective resistance of the tank circuit-sample system respectively, the phase angle $\alpha$ between the drive current $I_{rf}$ and the tank voltage $U$ is given by

$$\tan \alpha = \frac{1}{R_{eff}(H_{dc})} \left(\frac{1}{\omega C_T} - \omega L_{eff}(H_{dc})\right).$$  \hspace{1cm} (1)
It follows from Eq. 1 for $H_{dc} = 0$ and at the resonance frequency $\omega_0 = 1/\sqrt{L_{eff}(0)C_T}$ that the parameter $\alpha$ is zero. Therefore, by monitoring $\alpha$ as a function of $H_{dc}$ at the frequency $\omega_0$, the $L_{eff}(H_{dc})$ dependence can be obtained (note that $R_{eff}(H_{dc})$ dependence is controlled independently, by measuring the quality factor $Q$ of the tank circuit-sample system). If $R_{eff} = R_T$ does not depend on $H_{dc}$ then $\tan \alpha$ can be written as:

$$\tan \alpha = -k^2 Q \chi_m$$  \hspace{1cm} (2)

where $k$ is the coupling coefficient between the tank coil and the sample, and $\chi_m$ is ac magnetic susceptibility of the sample. In the experiments we are obviously interested in the regime $\chi_m \neq \text{const}$, the only configuration able to provide significant information. Let us analyze Eq. 2 near $H_e = 0$. When the supercurrent induced by an externally applied field is diamagnetic, a change of $\chi_m < 0$ will result in a local maximum in $\alpha(H_e)$. Similarly, a local minimum of the $\alpha(H_e)$ curve indicates a paramagnetic response ($\chi_m > 0$).

The simplest system which exhibits a similar behavior is the well-known rf SQUID. The sensor of this device is a Josephson junction inserted in a superconducting loop. If the inductance $L$ of the loop is relatively small (so that $\beta < 1$), the $\alpha(H_{dc})$ dependence has a local maximum at $H_{dc} = 0$ (see for example Ref. 11). Due to the induced current in the sensor, the magnetic flux $\Phi_1$ inside the loop satisfies $\Phi_1 < \Phi_e$, where $\Phi_e$ is an applied external flux. Therefore, the magnetic response is diamagnetic. If, instead of a conventional junction, a $\pi$-contact is inserted in the same sensor, the $\alpha(H_{dc})$ dependence has a local minimum at $H_{dc} = 0$ and $\Phi_1 > \Phi_e$, providing a paramagnetic response. The phase shift $\alpha$ can be obtained from Eq. 2 defining $\chi_m = d\Phi_1/d\Phi_e - 1$. The value of $k^2 Q$ allows the estimation of the resolution of the rf measurement, in this case of the order of a few percent of the flux quantum.

As we discussed above, within the framework of the $d$-wave scenario, extrinsic effects such as facetting can play a relevant role in the determination of the properties of the junctions and can contribute in particular to causing spontaneous currents and/or a paramagnetic effect. In the case of a strongly meandering interface, the GB exhibits a random parallel array of 0- and $\pi$-contacts. This is somehow the analog of the explanation of the PME in BiSCCO crystals in the 1-dimensional case of a GB line ($\pi$-loops model). An alternative mechanism of the PME can be given in terms of the midgap states (MGS) and surface properties of $d$-wave superconductors (MGS model). In this case, the MGS model is valid even for flat interfaces of a $d$-wave superconductor.

The interplay between the PME and superconductivity, apart from being an interesting topic itself on $d$-wave induced effects, may be crucial to improve understanding of transport properties of GBs. It has been demonstrated that GB transport properties strongly depend on the quality of the substrate of the thin film and the type of growth. This led to apparently conflicting behaviors in a wide spectrum of transport regimes. Zig-zag Nb-Au-YBCO junctions isolated the effect of facets by investigating the presence of spontaneous currents and anomalous magnetic patterns. We intend to reach the other limit by investigating a morphology with nominal very reduced faceting, and low barrier transparency. To this aim we employed biepitaxial junctions, where “clean” basal plane GBs can be reproducibly obtained.

The biepitaxial technique allows the fabrication of various GBJs by growing different seed layers and using substrates with different orientations. In this experiment we have used CeO$_2$ as a seed layer material deposited on (110) SrTiO$_3$ substrates. Details of the fabrication procedure can be found elsewhere. YBCO grows along the [001] direction on CeO$_2$ seed layers, while it grows along the [103]/[013] direction on SrTiO$_3$ substrates. By using CeO$_2$ as a seed layer we were able to induce a $45^\circ$ rotation of the a – b plane of the YBCO with respect to the in-plane direction of the SrTiO$_3$ substrate, and as a consequence the $\pi$ contact is formed. The measurements shown below are for the case where a $45^\circ$ c-axis tilt accompanies the $45^\circ$ a-axis tilt (Fig. 1a). This configuration in principle leads to interfaces where effects due to facetting can be very reduced, as shown for instance in the Scanning Electron Microscope image of Fig. 1b, and the relative sketch Fig. 1c. For biepitaxial junctions in the tilt case, the YBCO growth kinetics and the junction interface orientation determine that the long side of the [103] grains faces the c-axis counter-electrode, and this leads to a more controlled GB (basal plane GB). This has been confirmed by cross section Transmission Electron Microscope investigations.

FIG. 1: a) Sketch of the investigated biepitaxial grain boundary where a $45^\circ$ c-axis tilt accompanies the $45^\circ$ a-axis tilt; in b) a Scanning Electron Microscope image relative to the this GB is shown. The elongated grains on the left typical of the (103) growth may generate clean interfaces with reduced faceting, as evident also by the sketch in c).
to about 60 μm.

Results of rf measurements as a function of an externally applied magnetic field at the temperature range from T = 4.2 K up to 40 K are presented in Fig. 2 for nominally zero field cooled samples (the rest field is below 0.2 mOe). The sharp minimum at $H_{dc} = 0$ in Fig. 2 represents an unusual feature with respect to most GB systems, which exhibit a maximum for zero field. The minima at a finite magnetic field are originated by the redistribution of the magnetic flux into the GB as extensively discussed in Ref. 17.

According to the discussion above, the minimum of $α$ at $H_{dc} = 0$ is direct evidence of paramagnetic behavior of this type of GB. Furthermore the paramagnetic response was absent after the removal of YBCO from the GB region, demonstrating that the effect is only due to the GB. In other words we just repeated the same measurement on the same sample after removing only a narrow region of YBCO along the grain boundary line in order to prove that the paramagnetic signal was caused by the grain boundary and not by any uncontrolled environmental reason (substrate or sample holder) or possible impurities in the YBCO thin film far from the GB line.

The absence of hysteresis for $α(H_{dc})$-dependence with respect to external field means that there is no spontaneous surface current or flux generated in the GB. This is analogous to the situation in rf SQUID with $π$-contact for $β < 1$. As a matter of fact, in the case of finite fluctuations the jumps of $Φ_x$ can occur with a certain probability when $Φ_x$ falls in a hysteresis region. When the distribution width of the jump probability is larger than the width of the hysteresis, the flux jumps many times during the measurements. As a result the apparent time-averaged $Φ_x$ dependence presents a finite slope rather than hysteresis even for $β > 1$ (see Fig. 3). This situation has already been observed experimentally.

A detailed insight into the problem of the paramagnetic effect and of spontaneous currents in faceted GB’s has been given in Refs. 20, 21. In this model the current density $j_x(x)$ (x is the coordinate in the plane of the contact) is a random and alternating function of $x$, $j_x(x) = \langle j_x \rangle [1 + g_0 f(x)]$ with $\langle f(x) \rangle = 0$, $\max[ f(x)]=1$ and $g_0 = \max[ j_x(x)/\langle j_x \rangle]$. The length scale $l$ of $g(x)$ variations is of the order of the grain boundary meandering, typically $l$ is in the range of 0.01-0.1 μm 21. For a conventional current-phase relationship $j_x(x) = \langle j_x \rangle \sin(\varphi)$, the properties of the GBJJ are determined by the parameter $\gamma = g_0^2/l^2/8\pi^2 L^2_j$. Here $L_j = (e\Phi_0/16\pi^2\lambda(j_x))^1/2$ is the effective Josephson penetration depth and $\lambda$ is the London penetration depth. Within this model, for $γ < 1$ there is no created flux in GBJJ and the microjunctions stay in a “excited current-less state” 22. In principle, such junctions can exhibit a paramagnetic response. When $γ > 1$ there is flux generated in the GBJJ. Qualitatively, this requirement is similar to the condition $β > 1$ for the rf SQUID, as discussed above. Thus the same arguments concerning thermal fluctuations can be done for our experiments. If $Φ_x = 0$ and $T = 0$ there is spontaneous flux in the GB, one should observe hysteresis of the $Φ_x$ dependence (see Fig. 3, curve 1). However, at finite temperature fluctuations wash out the hysteresis, therefore there is no spontaneous current (see Fig. 3, curve 2). The above scenario relies on a macroscopic approach to the GB, which is a random array of parallel 0 and $π$-junctions, i.e. the “extrinsic” effect of faceting.

The other possible scenario is based on microscopic arguments, and mainly on mechanisms based on Andreev reflection at the surface 23,24,25,26. The $d$-wave symmetry of the gap leads to the formation of the surface state at zero energy (so-called midgap states - MGS). This MGS is degenerate with respect to the direction along the surface of the superconductor ($\pm k_y$). Any mechanism which is able to split the MGS will lower the energy of the system. The splitting of the MGS leads to spontaneous currents along the surface and therefore to time reversal symmetry breaking.

Different mechanisms of the MGS splitting were proposed in the literature (see Ref. 26 and Refs. therein). Apart from suggestions based on the presence of an imaginary component of the order parameter (like $d \pm is$, see for example Ref. 24), there are at least two scenarios based only on a pure $d$-wave symmetry of order parameter.

The first scenario takes into account the Josephson effect. For asymmetric 45° GBJJ the energy of the MGS can be written as

$$\varepsilon_{MGS}(\varphi, k_y) = -\text{sgn}(k_y) E_0(\vartheta)\sin(\varphi),$$

where $E_0 = ∆_{L} |\Delta_{R}| D(\vartheta)/(2(\Delta_{L} + D(\vartheta)||\Delta_{B}|| - |\Delta_{L}|)$, $D(\vartheta)$ is the angle-dependent barrier transparency and $∆_{L}$, $∆_{R}$ are superconducting energy gaps for the angle $\vartheta = \arcsin k_y/k_F$ in the left and right superconductor, respectively. For asymmetric 45° GBJJ the Josephson effect

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produce a gap oriented HTS surface due to the existence of the MGS. Hence, the spontaneous paramagnetic current flows in the surface layer \( \sim \psi \). This current is screened by the Meissner supercurrent on the scale of \( \lambda \) and the system pays for the gain in the Josephson energy at the expense of the energy of the magnetic field.

Within the framework of the second scenario the free surface of a \( d \)-wave superconductor has been found to be responsible for the appearance of the paramagnetic effect. In this case the paramagnetic quasi-particle current tries to compensate the Meissner supercurrent. As a matter of fact the supercurrent causes a redistribution of quasiparticles in \( \mathbf{k} \)-space due to the shift \( E_{\mathbf{k}} = E_{\mathbf{k}0} + \mathbf{p}_\mathbf{k} \cdot \mathbf{v}_s \) in the quasiparticle excitation energy, where \( E_{\mathbf{k}0} \) is the excitation energy in the absence of a supercurrent, \( \mathbf{v}_s \) is the velocity of the supercurrent and \( \mathbf{p}_\mathbf{k} \) is momentum of the quasiparticle. This is obviously relevant for a (110) oriented HTS surface due to the existence of the MGS.

The key feature for both of the described approaches is the presence of a mechanism able to split the MGS and produce a gap \( E_0 \), or in other words to populate the \( \pm k_y \) MGS unequally. This phenomenon is accompanied by a phase transition to a broken time reversal symmetry (TRSB) state. The transition temperature \( T_{\text{TRSB}} \) can be evaluated and in both approaches \( T_{\text{TRSB}} \) have been estimated to be below 1 K, in agreement with tunneling experiments. \( T_{\text{TRSB}} \) will be apparently the relevant parameter also for the PME. However, in analogy with \( rf \) SQUID properties, above \( T_{\text{TRSB}} \) one should observe no hysteresis but steep slope of \( \Phi_S(\Phi_e) \) at \( \Phi_e = 0 \) (again see Fig. 3). This explains why we observed PME in a wide temperature range well above the \( T_{\text{TRSB}} \) values but no hysteretic behavior.

Additional information has been provided by SSM investigations, which revealed the absence of spontaneous currents, as shown in the SSM images of the GBJJ region in Fig. 4 (a) and Fig. 4 (b) are SSM images of a wide area around the GB in zero field cooling, and in non-zero field cooling respectively, both at \( T = 4.2 \) K. Figure 4 (a) confirms in zero field cooling the absence of any spontaneous magnetization for this sample. This result is different from other measurements on \( 45^\circ \) asymmetric bicrystal and biepitaxial GBJJ. We attribute this difference to the concomitance of reduced faceting along the GB and the low barrier transparency of this junction, characterized by low values of the critical current density \( j_c \) about \( 10^5 \) A/cm\(^2\). Fig. 4 (b) gives evidence of vortices in both the electrodes, and in particular of anisotropic vortices in the (103) electrode. As a consequence, it seems to be not the case that the PME is originated by \( \pi \)-loops across the GB (\( \pi \)-loops model, see above).

Moreover, the observed narrow dip on \( J \) vs. \( H \) characteristics at \( H_{dc} = 0 \) requires \( \gamma \approx 1 \). Simple estimations show that \( \gamma \approx 1 \) corresponds to critical current densities across the GBJJ of the order of \( 10^5 \) A/cm\(^2\), which seems to be unrealistic, given that the average critical current density for our junction are of the order of \( 10^2 \) A/cm\(^2\). On the other hand the MGS model is apparently consistent with our results.

In conclusion, we have measured the magnetic-field response of an asymmetric \( 45^\circ \) grain boundary in a YBa\(_2\)Cu\(_3\)O\(_x\) thin film. The results of these investigations allow us to identify Andreev bound states as the cause of the paramagnetic effect, confirming theoretical predictions. Andreev bound states have been studied in detail theoretically in HTS Josephson junctions and systems. However, due to their extreme localization and stringent survival conditions, experimental detection has been basically confirmed only by one type of measure-
ment, zero bias anomalies in tunneling spectra. Our method is complementary and direct, and relies on the comparison of various types of measurements realized on the same samples. The contribution to the existing state of knowledge on d-wave order parameter symmetry in HTS superconductors is to demonstrate experimentally the occurrence of bound states through an innovative approach, shedding light on the paramagnetic effect in a novel topological configuration.

A paramagnetic response at low external fields was found in a zero-field-cooling regime. We have shown that the observed phenomena can be explained by the paramagnetic response of MGS surface currents.

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