Comment on “Energy levels, oscillator strengths, and transition probabilities for sulfur-like scandium, Sc VI” by El-Maaref et al. [Indian J. Phys. 91 1029 (2017)]

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Abstract: In this comment, through our independent calculations, we assess that the recently reported results of El-Maaref et al. [Indian J. Phys. 91 1029 (2017)] for energy levels, oscillator strengths, radiative rates, and lifetimes are inaccurate and unreliable for several levels and transitions of S-like Sc VI.

Keywords: Energy levels; Oscillator strengths; Lifetimes; S-like scandium Sc VI

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1. Introduction

Scandium (Sc) belongs to the group of rare earth elements and hence atomic data for its ions are useful for the studies of fusion plasmas [1]. It is also an important element for the studies of astrophysical plasmas, as discussed by Pryce [2], and is a key element for understanding Am stars, as demonstrated by LeBlanc and Alecian [3]. For this reason, several workers have reported atomic data for its ions—see for example, the early extensive work of Massacrier and Artru [4], who have reported atomic data for several ions of this element, i.e. Sc III to Sc XXI.

In one of the recent papers, El-Maaref et al. [5] have reported results for energy levels, oscillator strengths (f-values), radiative rates (A-values), and lifetimes (τ) for one of the important ions, namely S-like Sc VI. For the calculations, they have adopted two independent atomic structure codes, namely the configuration interaction version 3 (CIV3 [6]) and the Los Alamos National Laboratory (LANL) code, which is mainly based on the relativistic Hartree–Fock code of Cowan [7]. Based on these two calculations, and comparisons made with the existing theoretical and experimental results, they have assessed their data to be accurate and useful for applications. However, we strongly disagree with their calculations and conclusions, as discussed below.

For most levels, the differences between the CIV3 and LANL energies are ~2% (or ~8000 cm⁻¹ in absolute values), but up to 5% for a few, such as of 3p⁴ 3P₁₂—see table 2 of [5]. Since measurements of energies have also been made for some levels of Sc VI, these values have been compiled and assessed by the NIST (National Institute of Standards and Technology) team, and their recommended results are freely available at their website: https://physics.nist.gov/PhysRefData/ASD/levels_form.html. The measured energies are (generally) considered to be more accurate and, therefore, the aim of most calculations is to match their results with those. Therefore, as expected, El-Maaref et al. [5] have also made comparisons between their calculated energies and those listed by NIST. For lower levels, such as 1–9 (see table 2 of [5]), the CIV3 results are comparatively more accurate, but for the higher ones, such as 48–55, the LANL energies are in (much) better agreement with those of NIST. Therefore, there is no consistency.

Unfortunately, experimental energies are not available for all the levels calculated by El-Maaref et al. [5], and neither are the theoretical ones, as may be noted from their table 2. However, it is not strictly true, because as stated earlier, Massacrier and Artru [4] have considered much larger number of levels, i.e. 1889, more than an order of magnitude than those calculated by El-Maaref et al., i.e.

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only 160. They could not make comparisons with the earlier work as perhaps they were unaware of it. Anyway, it is not our (great) concern at present about the number of levels or their accuracy. However, based on the comparisons made by El-Maaref et al. or the ones briefly discussed by us above, we can state with confidence that there is scope for improvement in the calculated energies for the levels of Sc VI. But it may also be fair to state that there are no (large) discrepancies in their calculated energies. Therefore, we do not elaborate much on the energy levels or their accuracy. However, based on the comparisons we have preferred the choice of extended average level (EAL) in which a weighted (proportional to 2j+1) trace of the Hamiltonian matrix is minimised. This option produces a compromise set of orbitals describing closely lying states with moderate accuracy, and results obtained with other options, such as average level (AL), are comparable for all levels.

El-Maaref et al. [5] have considered 160 levels belonging to 8 configurations, namely 3s23p4, 3s3p5, 3s23p33d, 3s23p34s/4p/4d, and 3s23p5s/5p. In the calculations they have included limited CI, mainly among these 8 configurations. We have performed several calculations, gradually increasing the number of orbitals and configurations, and subsequently the CI. Our final calculations include 4498 levels, which belong to 41 configurations, namely 3s23p4, 3s3p5, 3p6, 3s3p33d, 3s3p43d, 3p53d, 3s2p33d2, 3s3p33d2, 3s23p34f, 3s3p44f, 3s3p323d4f, 3s23p33d4f, 3s3p33d4f, 3p3d2, 3p54f, 3s3p23d2, 3s23p5f, and 3s23p5f (l ≤ g). Inclusion of such a large CI is necessary for two reasons: (i) Sc VI is only moderately heavy and, more importantly, (ii) levels of these configurations intermix—see for example table 5 of Massacrier and Artru [4]. El-Maaref et al. have ignored many of the important configurations, such as 3s3p43d whose 56 levels appear early on, well before those of 3p34f. Another example is 3p6, which generates only one level but intermixes with those of 3p33d. El-Maaref et al. have mostly included those configurations whose energy levels appear on the NIST website. Inclusion of these additional configurations not only improves the accuracy of the calculated energies but also (significantly) affects the further determinations of τ, because contributions arising from these missing levels are also accounted for. Conversely, the 160 levels considered by them are not the lowest. To calculate lifetime for the highest level of their calculations, i.e. 3p15p 1S0, one needs to consider at least 524 levels!

2. Calculations

For the determination of energy levels, radiative rates, oscillator strengths, and lifetimes, we have adopted the General-purpose Relativistic Atomic Structure Package (GRASP). The original code, developed by Grant et al. [9], has undergone numerous modifications and improvements by many workers in the past, and as a result of it several published versions are available in the literature, but the one employed by us is known as GRASP0 and is currently hosted at the website http://amdpp.phys.strath.ac.uk/UK_APAP/codes.html. This is a fully relativistic code based on the jj coupling scheme, although the two-body relativistic operators included in this (but not in CIV3) are not too important for a moderately heavy ion Sc VI. Therefore, differences (if any) in energies (or other related parameters) with other calculations will not be because of this, but for other reasons. Finally, in the calculations, we have preferred the choice of extended average level (EAL) in which a weighted (proportional to 2j+1) trace of the Hamiltonian matrix is minimised. This option produces a compromise set of orbitals describing closely lying states with moderate accuracy, and results obtained with other options, such as average level (AL), are comparable for all levels.

As stated in Sect. 1, our focus is on the results for f- (or A-) values. For weaker transitions (say with f < 0.1), differences among different calculations may sometimes be considerably large, particularly for those with f < 10⁻³. This is because their resultant matrices are highly sensitive to the small mixing coefficients from different levels and
configurations. However, comparatively stronger transitions are generally immune to the additive or cancellation effects of the coefficients, because of their larger magnitudes. Therefore, it is much easier to establish the (in)accuracy of a calculation for such transitions by comparing their \( f \)-values.

In Table 1 we list a few transitions which are comparatively strong(er) with \( f \)-values from the CIV3 calculations of El-Maaref et al. [5], Froese Fischer et al. [8] with MCHF, and our own work with GRASP. These representative transitions are sufficient to highlight the similarity (and or the discrepancies) among different calculations. For all transitions listed here (and many more—see table A of [10]) there is a satisfactory agreement between the MCHF and GRASP results, but the CIV3 \( f \)-values of El-Maaref et al. differ by up to three orders of magnitude. Clearly, the results of El-Maaref et al. are neither correct nor reliable.

4. Lifetimes

The lifetime of a level is determined as \( \tau (s) = 1.0/\Sigma A_{ji} \) where the summation runs over all types of transitions, although the electric dipole (E1) ones are normally the most dominant in magnitude, and hence more important. Nevertheless, we have included contributions from other types as well, namely magnetic dipole (M1), electric quadrupole (E2), and magnetic quadrupole (M2), which have been ignored by El-Maaref et al. [5], but have also been considered by Froese Fischer et al. [8], as expected.

In Table 2 we list only those levels for which differences between the CIV3 and MCHF values of \( \tau \) are very large, i.e. up to three orders of magnitude. Furthermore, for brevity, only the lowest few levels are considered here.

| Lower level | Upper level | CIV3 | MCHF | GRASP |
|-------------|-------------|------|------|-------|
| 3p\(^4\) \( ^3\)P\(_2\) | 3p\(^3\)\(^2\)P\(_3\) \( ^3\)P\(_2\) | 0.148 | 0.018 | 0.016 |
| 3p\(^4\) \( ^1\)P\(_1\) | 3p\(^3\)\(^2\)D\(_3\) \( ^3\)P\(_1\) | 0.006 | 0.792 | 0.771 |
| 3p\(^4\) \( ^1\)P\(_2\) | 3p\(^3\)\(^2\)D\(_3\) \( ^1\)P\(_2\) | 6.74 | 0.183 | 0.161 |
| 3p\(^4\) \( ^3\)P\(_2\) | 3p\(^3\)\(^3\)S\(_3\) \( ^3\)D\(_3\) | 0.589 | 1.480 | 1.490 |
| 3p\(^4\) \( ^1\)P\(_1\) | 3p\(^3\)\(^3\)S\(_3\) \( ^1\)D\(_3\) | 0.106 | 0.231 | 0.238 |
| 3p\(^4\) \( ^3\)P\(_1\) | 3p\(^3\)\(^3\)S\(_3\) \( ^3\)D\(_2\) | 0.178 | 1.360 | 1.364 |
| 3p\(^4\) \( ^1\)P\(_0\) | 3s3p\(^5\) \( ^3\)P\(_0\) | 0.102 | 0.056 | 0.052 |
| 3p\(^4\) \( ^3\)P\(_0\) | 3p\(^3\)\(^3\)D\(_3\) \( ^3\)P\(_1\) | 0.003 | 0.831 | 0.953 |

Table 1: Comparison of oscillator strengths (\( f \)-values) for some transitions of Sc VI. \( a \pm b \equiv a \times 10^{10} \)

Table 2: Comparison of lifetimes (\( \tau \), s) for some levels of Sc VI. \( a \pm b \equiv a \times 10^{10} \)

| Level | CIV3 | MCHF | GRASP |
|-------|------|------|-------|
| 3p\(^3\)\(^2\)P\(_3\) \( ^3\)P\(_2\) | 2.25–10 | 2.50–09 | 1.59–09 |
| 3p\(^3\)\(^1\)P\(_3\) \( ^3\)P\(_1\) | 1.51–10 | 1.86–09 | 8.91–10 |
| 3p\(^3\)\(^2\)P\(_3\) \( ^1\)P\(_2\) | 8.02–11 | 8.66–10 | 5.49–10 |
| 3p\(^3\)\(^1\)D\(_3\) \( ^3\)P\(_2\) | 1.71–09 | 1.28–11 | 1.25–11 |
| 3p\(^3\)\(^1\)D\(_3\) \( ^1\)P\(_0\) | 5.12–09 | 1.29–11 | 1.26–11 |
| 3p\(^3\)\(^1\)D\(_3\) \( ^3\)P\(_0\) | 1.05–08 | 1.25–11 | 1.22–11 |

CIV3: earlier calculations of El-Maaref et al. [5] with the civ3 code
MCHF: earlier calculations of Froese Fischer et al. [8] with the mchf code
GRASP: present calculations with the grasp code

Agreement between the GRASP and MCHF calculations is generally highly satisfactory and is within a factor of two. These differences are understandable, because \( f \)-values for most of these levels are rather small in magnitude. However, discrepancies with the corresponding CIV3 results of El-Maaref et al. [5] are indeed very large, and have arisen because of the corresponding differences in the \( f \) - (and \( A \) )-values, noted in Sect. 3.

5. Conclusions

In a recent paper, El-Maaref et al. [5] have reported results for energy levels, \( f \)-values, \( A \)-values, and \( \tau \) for the levels/transitions of S-like Sc VI. Most of their results are based on the CIV3 calculations. While their calculated energies are (nearly) acceptable for most levels, the corresponding results for other parameters are not, because these differ from the earlier available as well as our present work for several transitions, by up to three orders of magnitude. The main reason for such large discrepancies is the inclusion of limited (and arbitrary) CI in their work. Much more accurate, and larger, calculations already exist in the literature, which are by Froese Fischer et al. [8] and Massacrier and Artru [4], respectively. However, there is still scope for further improvement as well as extension over the existing results. This is because levels of Froese Fischer et al. are confined to those of the \( 3s^33p^4 \), \( 3s3p^5 \) and \( 3s^23p^33d \) configurations only. Massacrier and Artru, on the other hand, have included considerably larger CI (among 51 configurations) and have reported data for 1889 levels, but their results for \( A \)-values are confined to the E1 transitions alone, whereas those with other types (E2, M1 and M2) are also desirable in the modelling of plasmas, and particularly in the determination of lifetimes. Therefore, in a recent paper [10], we have reported a complete set of data
for all levels and their transitions, not only for S-like Sc VI, but also for V VIII, Cr IX, and Mn X.

With the easy access to atomic structure (and scattering) codes, it has become (rather) straightforward to generate atomic data for various parameters. However, such data may not be of any use and may often be confusing and misleading, because generating accurate and reliable data, which can be confidently applied for modelling or diagnostics of plasmas, is still difficult to produce as several checks and comparisons are required, particularly when the earlier available results are in paucity. This is the main reason that large discrepancies, of orders of magnitude, are often observed in the reported data (for any ion), as noted here for Sc VI and highlighted earlier for many others in our earlier publications [11, 12]. Finally, for the benefit of the readers, we will like to note that the earlier reported results by El-Maaref and co-workers are in large errors for other ions also, as discussed and explained by us for S-like Mn X [13], Kr-like W XXXIX [14] and Zn-like W XLV [15].

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