Heavy fermion spin liquid in herbertsmithite

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We analyze recent heat capacity measurements in herbertsmithite ZnCu$_3$(OH)$_6$Cl$_2$ single crystal samples subjected to strong magnetic fields. We show that the temperature dependence of specific heat $C_{mag}$ formed by quantum spin liquid at different magnetic fields $B$ resembles the electronic heat capacity $C_{el}$ of the HF metal YbRh$_2$Si$_2$. We demonstrate that the spinon effective mass $M_{mag} \propto C_{mag}/T$ exhibits a scaling behavior like that of $C_{el}/T$. We also show that the recent measurements of $C_{mag}$ are compatible with those obtained on powder samples. These observations allow us to conclude that ZnCu$_3$(OH)$_6$Cl$_2$ holds a strongly correlated quantum spin liquid, and a possible gap in the spectra of spinon excitations is absent even under the application of very high magnetic fields of 18 T.

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Quantum spin liquids (QSLs) are promising new phases, where exotic quantum states of matter could be realized. Although much theoretical effort has been devoted to understand their physical nature, the question is still far from its complete clarification. Generally speaking, the QSL is a quantum state, formed with hypothetic particles like fermionic spinons carrying spin 1/2 and no charge. A number of QSLs with various types of ground states are proposed [1–18] but the lack of real materials possessing them obscure the underlying physical mechanism. On the other hand, one needs a real theory that plays important role in the understanding and interpreting accessible experimental facts [19–22]. Measurements on magnetic insulators with geometrical frustration produce important experimental data shedding light on the nature of spinon composing QSL. Recent measurements indicate that the insulator ZnCu$_3$(OH)$_6$Cl$_2$ (herbertsmithite) is very likely to be the first promising candidate to host a QSL in real bulk materials. In herbertsmithite, the dynamic magnetic susceptibility shows that at low temperatures quasiparticle excitations, or spinons, form a continuum, and populate an approximately flat band crossing the Fermi level [17, 21]. At the same time, our analysis of herbertsmithite thermodynamic properties allows us to reveal their scaling behavior. The above results demonstrate that the properties of the herbertsmithite are similar to those of heavy-fermion (HF) metals. Thus, it can be viewed as a new type of strongly correlated HF electrical insulator exhibiting properties of HF metals but resisting electric current [20, 22].

The development of this concept, however, faces fundamental problems still remaining to be resolved. The first one is that the experimental data are taken in measurements on herbertsmithite powder samples [4–6, 20–22]. As a result, both out-of-plane magnetic defects and site disorder between the Cu and Zn ions can strongly change the behavior of the bulk susceptibility or even alter its low-temperature scaling at weak magnetic fields, see e.g. Ref. [16]. The second problem is based on experimental data showing that QSL in the herbertsmithite is unstable against the application of external magnetic fields. This instability is represented by the emergence of so-called spin-solid phase, which, in turn, is separated from the spin-liquid one by a gap induced by an applied magnetic field [22]. Thus, the experimental observations of QSL remain scattered and need regimentation. In our opinion, this can be partially achieved by presenting a reliable interpretation of the recent measurements of specific heat $C$ in high magnetic fields performed on herbertsmithite single crystal samples [24, 25].

In this Communication we analyze the recent heat capacity $C$ measurements in strong magnetic fields on herbertsmithite. We interpret the above measurements in terms of QSL spinon contribution. To obtain the spinon - determined partial specific heat $C_{mag}$, we subtract the phonon and Schottky effect contributions from the total heat capacity $C$. It turns out that obtained $C_{mag}$ as a function of temperature $T$ at fixed magnetic field $B$ behaves very similarly to the electronic specific heat $C_{el}$ of the HF metal YbRh$_2$Si$_2$. This observation allows us to conclude that spinons form the Fermi sphere with the Fermi momentum $p_F$, while the gap in the spectra of spinon excitations and the spin-solid phase are absent. We demonstrate that the effective mass of spinon $M_{mag} \propto C_{mag}/T$ exhibits a scaling behavior resembling that of $C_{el}/T$. We also show that new measurements of $C_{mag}$ on single crystal samples are compatible with those obtained on powder samples.

The $S = 1/2$ spins of the Cu$^{+2}$ ions occupy the positions in a highly symmetric kagome lattice. As spins on
the above lattice reside in a highly symmetric structure of corner-sharing triangles, the ground state energy does not depend on the spins configuration. As a result, spins located at the kagome hexagon, composed of the two triangles, form a (frustrated) pattern that is even more frustrated than the triangular lattice considered by Anderson. As a result, the kagome lattice has a flat topologically protected branch of the spectrum with zero excitation energy. Therefore, the fermion condensation quantum phase transition (FCQPT) can be considered as a quantum critical point (QCP) of the ZnCu$_3$(OH)$_6$Cl$_2$ QSL. In that case, we expect that at low temperatures the heat capacity $C$ of herbertsmithite becomes a function of the applied magnetic field, as it is seen from Fig. 1. We propose that mentioned QSL is composed of chargeless fermions called spinons with the effective mass $M_{mag}^*$. Latter fermions with spin $\sigma = 1/2$ occupy the corresponding Fermi sphere with the Fermi momentum $p_F$, and form the excitation spectrum typical for HF liquid located near FCQPT, while spinons represent HF quasiparticles of deconfined QSL. Thus, the ground state energy $E(n)$ is given by the Landau functional depending on the spinon distribution function $n_{\sigma}(p)$, where $p$ is the momentum. Near FCQPT point, the effective mass $M_{mag}^*$ is governed by the Landau equation

$$\frac{1}{M_{mag}^*(T,B)} = \frac{1}{M_{mag}^*(T = 0, B = 0)} + \frac{1}{p_F^2} \sum_{\sigma_1} \left( \frac{\delta n_{\sigma_1}(p_F)}{\gamma_1} \right) \frac{\partial^2 C_{mag}(T,B)}{\partial p_{\sigma_1}^2} (2\pi)^3. \tag{1}$$

Here we have rewritten the spinon distribution function as $\delta n_{\sigma}(p) = n_{\sigma}(p,T,B) - n_{\sigma}(p,T = 0, B = 0)$. The Landau interaction $F$ is defined by the fact that the system has to be at FCQPT. Thus, this interaction brings the system to FCQPT point, where Fermi surface alters its topology so that the effective mass acquires temperature and field dependence. At this point, the term $1/M_{mag}^*(T = 0, B = 0)$ vanishes and Eq. (1) becomes homogeneous. It can then be solved analytically. At $B = 0$, the effective mass depends on $T$ demonstrating the NFL (non-Fermi liquid) behavior

$$M_{mag}^*(T) \approx a_T T^{-2/3}. \tag{2}$$

At finite $T$, the application of magnetic field $B$ drives the system to Landau Fermi liquid (LFL) region with

$$M_{mag}^*(B) \approx a_B B^{-2/3}. \tag{3}$$

At finite $B$ and $T$ near FCQPT, the solutions of Eq. (1) $M_{mag}^*(B,T)$ can be well approximated by a simple universal interpolating function. The interpolation occurs between the LFL ($M^*(T) \propto \text{const}$) and NFL ($M_{mag}^*(T) \propto T^{-2/3}$) regions. As it is seen from Eq. (3), under the application of magnetic field $M_{mag}^*$ becomes finite, and at low temperatures the system demonstrates the LFL behavior $C_{mag}(T)/T \propto M_{mag}^*(T) \simeq M_{mag}^*(T = 0) + a_1 T^3$. Then, as it is seen from Fig. 2 at increasing temperatures $M_{mag}^* \propto C_{mag}(T)/T$ grows, and enters a transition regime, reaching its maximum $M_{max}^* \propto (C_{mag}(T)/T)_{max}$ at $T = T_{max}$, with subsequent diminishing given by Eq. (2).

To reveal a scaling behavior, we introduce the normalized effective mass $M_N^*$ and the normalized temperature $T_N$ dividing the effective mass $M_{mag}^*$ by its maximal values, $M_{max}^*$, and temperature $T$ by $T_{max}$ at which the maximum occurs. The normalized effective mass $M_N^* = M^*/M_{max}^*$ as a function of the normalized temperature $y = T_N = T/T_{max}$ is given by the interpolating function that approximates the solution of Eq. (1)

$$M_N^*(y) \approx c_0 + c_1 y^2 + c_2 y^3. \tag{4}$$

Here $c_0 = (1 + c_2)/(1 + c_1)$, $c_1$ and $c_2$ are fitting parameters, $c_1$ and $c_2$ are fitting parameters, parameterizing the Landau interaction. Magnetic field $B$ enters Eq. (1) only in the combination $\mu_B B/k_B T$, making $k_B T_{max} \simeq \mu_B B$ where $\mu_B$ is Boltzmann constant and $\mu_B$ is Bohr magneton. Thus, Eq. (1) exhibits the scaling behavior, which is the intrinsic property of Eq. (1) at FCQPT: $M_N^*$ at different magnetic fields merges into a single curve as a function of the variable $y$. In what follows we use Eq. (4) to clarify our calculations based on Eq. (1).

To analyze the spinon specific heat $C_{mag}(T,B)$, we have to exclude the contribution coming from lattice (phonons) that is independent of $B$. To separate $C_{mag}$ contribution, we approximate $C(T,B = 0)$ by the function

$$C(T) = a_T T^{1/3} + b T^3. \tag{5}$$
FIG. 2: (color online). Panel a: The specific heat \( C_{\text{mag}}/T \) of ZnCu\(_3\)(OH)\(_6\)Cl\(_2\) measured on powder [21, 25]. \( C_{\text{mag}}/T \) is displayed as a function of temperature \( T \) for fields \( B \) shown in the legends. Panel b: The specific heat \( C_{\text{el}}/T \) extracted from measurements on the HF metal YbRh\(_2\)Si\(_2\) [31] exhibits the same behavior as \( C_{\text{mag}}/T \). The illustrative values of the maxima \( C_{\text{mag}}/T \) and \( C_{\text{el}}/T \) of both \( C_{\text{mag}}/T \) and \( C_{\text{el}}/T \) and the corresponding \( T_{\text{max}} \) are also shown in panels a and b.

Here the first term proportional to \( M_{\text{mag}}^*(T) \propto T^{1/3} \) presents the QSL contribution when it exhibits the NFL behavior, as it follows from Eq. [2], while the second one is determined by the lattice (phonon) contribution. It is seen from Fig. 1 that the approximation [29] is valid in a wide temperature range. At low temperatures \( T \leq 4 \) K the heat capacity is mainly formed by spinons, while the phonon contribution prevails at higher temperatures, making its main contribution at \( T \geq 10 \) K. It is seen, that at diminishing temperatures the LFL behavior, \( C \propto T \), starts to form. We note, that the Schottky anomaly was removed, as it is usually done, see e.g. [24, 25]. Upon comparing the data on the heat capacity taken at \( B = 9 \) and \( B = 14 \) T shown in Fig. 1 one concludes that \( C \) strongly depends on the magnetic field. However, at raising temperatures \( T \geq 10 \) K the \( B \)-dependence vanishes, for the contribution coming from phonons prevails, then, the system enters the transition regime at \( k_B T \approx \mu_B B \), and the influence of magnetic field becomes weak, as shown in the \( T - B \) phase diagram, Fig. 3.

The obtained heat capacity of QSL, \( C_{\text{mag}}/T = (C - B T^3)/T \), is displayed in Fig. 2 panel a. It follows from panel a, that the results obtained on different kinds (powder and single crystal) of samples and in different measurements [4, 5, 24, 25] exhibit similar properties. To show that the behavior of \( C_{\text{mag}}/T \) reported in panel a is of generic character, we note that \( C_{\text{mag}}/T \propto M_{\text{mag}}^* \) behaves like \( C_{\text{el}}/T \) shown in panel b. Indeed, as seen from Fig. 2 the maximum structure in \( C_{\text{mag}}/T \) and \( C_{\text{el}}/T \) at temperature \( T_{\text{max}} \) appears under the application of magnetic field \( B \) and \( T_{\text{max}} \) shifts to higher \( T \) as \( B \) is increased. The value of the maximum structure is saturated towards lower temperatures decreasing at elevated magnetic fields. It is worthy to note, that \( C_{\text{mag}}/T \propto C_{\text{el}}/T \), as it is seen from the panels a and b. Thus, QSL of ZnCu\(_3\)(OH)\(_6\)Cl\(_2\) can be viewed as a strongly correlated quantum spin liquid (SCQSL) that behaves like that of the HF metal YbRh\(_2\)Si\(_2\), exhibiting a gapless behavior in high magnetic fields up to 18 T.

We now construct the schematic phase diagram of ZnCu\(_3\)(OH)\(_6\)Cl\(_2\), reported in Fig. 3 At \( T = 0 \) and...
The application of $B$ shifts $T_{\text{max}}$ to higher temperatures. On the contrary, at fixed magnetic field and increasing temperatures the system moves along the vertical arrow from the LFL to NFL region. The inset to Fig. 3 demonstrates the behavior of the normalized effective mass $M^*_N$ versus the normalized temperature $T_N$, as shown by the dashed line in Fig. 3. It is seen that the temperature range $T_N \sim 1$ represents the transition region between the LFL regime and the NFL regime with almost constant effective mass and the NFL behavior, having the $T^{-2/3}$ dependence. It follows from Eq. 4 and Fig. 3 that the width of the transition region is given by $T_M \sim T_{\text{max}}(B) \propto T \propto B$. The phase diagram in Fig. 5 demonstrates that the properties of ZnCu$_3$(OH)$_6$Cl$_2$ are close to those of the HF metal YbRh$_2$Si$_2$.

Figure 5 panel a, reports the normalized specific heat $(C_{\text{mag}}/T)_N = M^*_N$ versus normalized temperature $T_N$ as a function of $B$. It is seen that at low $T_N \lesssim 0.1$, $(C_{\text{mag}}/T)_N \approx 0.4$. This value is determined by the QSL polarization in magnetic fields, and coincides with that of $(C_{\text{el}}/T)_N = M^*_N$ obtained on YbRh$_2$Si$_2$. In both panels a and b, our calculations are shown by the same solid curve. Note that at low temperatures and magnetic fields, when the polarization is negligible, $C_{\text{el}}(T) \approx 0.9$, as it is seen from panel b of Fig. 4.

In Fig. 5 panel a, the solid squares denote the values of the maxima $(C_{\text{mag}}/T)_{\text{max}}(B)$, taken from Fig. 2 panel a. In panel b, the corresponding values of $T_{\text{max}}(B)$ are displayed versus magnetic field $B$. It is seen that the agreement between the theory and experiment is good. In panel b, the solid straight line represents the function $T_{\text{max}}(B) \propto d_2 B$. It is seen that at relatively high temperatures the experimental data are well approximated by the straight line, while at $T \leq T_d$ there is deviation.
This fact evidences that SCQSL of herbertsmithite is not exactly placed at FCQPT, for in that case the approximation \( T_{\text{max}} \propto d_2B \) would be good at low temperatures. This conclusion coincides with general properties of the phase diagrams of HF metals [27] and with experimental data, showing that at low temperatures \( C \) demonstrates the LFL behavior [5, 24, 25], see Fig. 1 as well.

In summary, based on the recent experimental facts, we have shown that ZnCu_3(OH)_6Cl_2 can be viewed as a strongly correlated Fermi system whose thermodynamics is defined by SCQSL located at FCQPT. Our calculations of the heat capacity \( C_{\text{mag}}/T \) are in good agreement with the experimental data and the scaling behavior of \( C_{\text{mag}}/T \) coincides with that observed in the HF metal YbRh_2Si_2 up to high magnetic fields of 18 T. Thus, spinons forming SCQSL remain itinerant even in high magnetic fields. We also have shown that recent measurements of \( C_{\text{mag}} \) on single crystal samples are consistent with those obtained on powder samples.

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