Discrimination of the Healthy and Sick Cardiac Autonomic Nervous System by a New Wavelet Analysis of Heartbeat Intervals

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We demonstrate that it is possible to distinguish with a complete certainty between healthy subjects and patients with various dysfunctions of the cardiac nervous system by way of multiresolutional wavelet transform of RR intervals. We repeated the study of Thurner et al on different ensemble of subjects. We show that reconstructed series using a filter which discards wavelet coefficients related with higher scales enables one to classify individuals for which the method otherwise is inconclusive. We suggest a delimiting diagnostic value of the standard deviation of the filtered, reconstructed RR interval time series in the range of $\sim 0.035$ (for the above mentioned filter), below which individuals are at risk.

I. INTRODUCTION

Measurement of heart rate (HR) and evaluation of its rhythmicity have been used for a long time as a simple clinical indicator. The main adaptive regulation of the sinus node function and thereby the HR, is exerted by the autonomic nervous system. The sinus node of the heart is a major organ in the integrated control of cardiovascular function. HR abnormality may therefore be an early or principle sign of disease or malfunction.

Research from the last decade indicates that a quantification of the discrete beat to beat variations in HR - heart rate variability (HRV) may be used more directly to estimate efferent autonomic activity to the heart and the integrity of this cardiovascular control system. The finding that power spectral analysis of HRV could be used as a marker of cardiac autonomic outflow to the heart, was considered a breakthrough for clinical research.

Autonomic dysfunction is an important factor in a number of conditions. In diabetes, an abnormality in autonomic nervous function signals an adverse prognosis and risk of subsequent heart disease. Recognition of early dysfunction is therefore important. In overt heart disease autonomic imbalance is of significant importance in the pathophysiology of sudden cardiac death. Abnormal autonomic balance is an important prognostic factor. In heart failure this control system may be significantly deranged.

Techniques which can discriminate the healthy HRV profile from a sick one are therefore highly desirable. So far this has not been accomplished, as a considerable overlap between healthy and sick, (i.e. healthy and diabetes) or high and low risk heart disease patients, have been reported. The time series used for HRV analysis are derived from 24-hour ECG recordings. These are clinically widely used and offer important additional information. However, several problems have limited the use and interpretation of the spectral analysis results. The ambulatory time segments inherently lack stationarity. Furthermore, they often include transients caused by artifacts, ectopic beats, noise, tape speed errors which may have significant impact on the power spectrum. This significantly limits the sensitivity of this technique, and thus may limit its applicability.

II. METHODS

One of the most successful techniques to analyze non-stationary time series is the Multiresolution Wavelet Analysis. This technique was recently utilized in order to analyze a sequence of RR intervals. Ref. identifies different scaling properties in healthy and sleep apnea patients. In a previous study, Peng et al were able to distinguish between healthy subjects and patients with heart failure by the use of the detrended fluctuation analysis. Later, Thurner et al used a similar procedure but focused on the values of the variance rather than on the scaling exponent. For the scale windows of $m = 4$ and $m = 5$ heartbeats, the standard deviations of the wavelet coefficients for normal individuals and heart failure patients were divided into two disjoint sets. In this way the authors of ref. succeeded to classify subjects from a test group as either belonging to the heart failure or the normal group, and that with a 100% accuracy.

The Discrete Wavelet transform is a mathematical recipe acting on a data vector of length $2^m$, $m = 1, 2, \ldots$ and transforming it into a different vector of the same length. It is based on recursive sums and differences of
We have, however, elaborated on the procedure applied in ref. [4] by utilizing a filter-technique. Thus we perform an Inverse Wavelet Transform, but retain only a specific scale in the reconstruction of the time series; a complete separation is observed for $m = 4$ or $m = 5$. In this way a reconstructed and filtered time series is obtained and a comparison with the original time series shows a substantial difference in amplitude between sick/healthy subjects relative to the difference found in the original RR interval time series. The choice of $m = 4$ or $m = 5$ was motivated by the findings in ref. [4] and by our own results.

### III. RESULTS

We have calculated the standard deviation $\sigma_{\text{wave}}$ for Daubechies 10-tap wavelet versus the scale $m$, $1 \leq m \leq 10$, for 33 persons. In accordance with ref. [4] we find that for $4 \leq m \leq 6$ the $\sigma_{\text{wave}}$ separate the two classes of subjects and hence provide a clinically significant measure of the presence of cardiac autonomic dysfunction with a 97% sensitivity. This supports in a convincing way the findings of ref. [4]. We have been able to confirm this trend with other wavelets.

The main result of this study is however the possibility to display the standard deviation of the RR interval amplitude vs. the beat number in the reconstructed, filtered time series. This standard deviation, here denoted by $\sigma_{\text{filter}}$, can be used to obtain a separation of sick/healthy subjects.

In fig. 1 we display the RR intervals vs. the beat number of a normal subject. The wavelet technique cleans the highest and lowest frequencies from the overall picture. The highest frequencies contain noise and the lowest frequencies contain mainly external influences on the HR pattern like movement and slower trends in HR level, which are not necessarily reflective of autonomic nervous activity. After the removal of these frequencies one is left with the characteristic frequencies of the heart.

Fig. 2 shows the standard deviation $\sigma_{\text{wave}}$ for a Daubechies 10-tap wavelet as a function of the scale number $m$. The almost total separation between sick and healthy subjects is obvious.

Patient #1, falling into the range of sick patients, has a very low HRV both on a 24-hour scale and short term. The patient is a survivor of a heart infarct and is at high risk of sudden cardiac death.

Patient #2 has the lowest $\sigma_{\text{wave}}$ values in the range $4 \leq m \leq 6$. He has undergone a heart transplant; the nerves to the heart have been disconnected and there is almost no HRV.

Patient #3 is a diabetic patient, who is classified by the wavelet technique as a high risk patient. Diabetic patients with abnormal cardiac autonomic function have an adverse prognosis and increased risk of heart disease.

Patient #4, also a diabetic, seems to be less at risk.
His $\sigma_{\text{wave}}$ is near the transition between healthy and sick subjects.

![Graph](image1)

FIG. 2. Daubechies 10-tap wavelet. $\sigma_{\text{wave}}$, the standard deviation, is plotted as a function of the scale $m$, $1 \leq m \leq 10$. The corresponding window size is $2^m$. The empty symbols indicate the healthy subjects, the opaque symbols indicate patients. The circles designate normal subjects, the squares - diabetic patients, diamond - patient at risk with heart infarct and triangle - a heart transplanted patient.

The method used in ref. [14] fails for subject #5, who appears in the risk group, although he had no evidence of diabetes or heart disease.

![Graph](image2)

FIG. 3. Daubechies 10-tap wavelet filtered inverse transform. The symbols are as in fig. 2.

In fig. 3 the standard deviation of the amplitude of the reconstructed time series has been calculated for $1 \leq m \leq 10$. Again, a total separation between sick and healthy subjects is apparent. The fact that the $\sigma_{\text{filter}}$ remain almost constant for scales between 4 and 6 for each individual hints to the possibility that the corresponding frequencies are characteristic of those at which the autonomic nervous system works.

![Graph](image3)

FIG. 4. (a) Typical time series segments for a sick and a normal individual. (b) Typical reconstructed, filtered time series for the above individuals. The segments shown are the same as in (a). The filter is created by the inverse transform of coefficients with scale $m = 4$.

Fig. 4a shows a typical RR interval time series for a healthy and a sick subject, whereas fig. 4b shows the reconstructed time series $(m = 4)$. One notices that the difference in amplitudes for healthy/sick subjects is much more pronounced in the latter time series.
FIG. 5. (a) and (b). The Fourier transforms of the above (fig. 4). An index of 1000 represents a frequency of 0.02 Hz.

Figs. 5a and 5b show the Fourier transforms for the time series displayed in figs. 4a and 4b, respectively. These power spectra appear similar, however differ in their respective order of magnitude. Clearly, the reconstructed filtered time series are distinct by the amplitude as well as the broadness of their Fourier transforms.

In fig. 6 we have obtained a complete separation between the sick and healthy subjects by application of a filter which is created by retaining wavelet coefficients with scales $1 \leq m \leq 6$. This filter was motivated by the observation that a separation is evident for these scales (see figs. 2a and 4b). One observes that the healthy subject #5, who failed the wavelet transform diagnostics of ref. [14] (fig. 2), is now properly classified as not being at risk.

FIG. 6. Daubechies 10-tap wavelet filtered inverse transform. The symbols are as in figs. 2. The filter is created by the inverse transform of coefficients with $1 \leq m \leq 7$.

IV. CONCLUSION

Our study supports the conjecture of ref. [14] that healthy subjects exhibit greater fluctuations (larger $\sigma_{wave}$ values) than patients. This difference in fluctuations becomes most evident on the scale 4 to 5 (corresponding to windows of 16 and 32 heartbeats), but in our study it is apparent at all scales from 1 to 7 (windows of 2 to 128 heartbeats).

The most distinct difference between sick and healthy individuals appears in the amplitude changes in the 'reconstructed' time series, where the windows of 16, 32 and 64 heartbeats contribute in a similar way. Letting the window be as small as $2^4$ heartbeats is enough to allow the healthy group to show substantial variation in the size of RR intervals implying a large $\sigma$ value, but is at the same time too small a window to let the sick cardiac autonomic nervous system introduce significant variations in the length of the RR intervals and hence allows it only to reach a $\sigma$ value essentially smaller than the healthy heart.

The final conclusion of this study is that in order to obtain a complete separation between healthy subjects and patients one has to consider a range of scales (as shown in fig. 6) instead of only one scale (as in figs. 2 and 3). This implies that, $\sigma_{filter}$ as in fig. 6 can be used as a diagnostic indicator, with a delimiting value of $\sim 0.035$ (for the above mentioned filter), below which the
persons have abnormal cardiac autonomic function and will be at risk.

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