Search for leptonic decays of $D^0$ mesons

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We search for the flavor-changing neutral current decays $D^0 \to \mu^+\mu^-$ and $D^0 \to e^+e^-$, and for the lepton-flavor violating decays $D^0 \to e^\pm\mu^\mp$ using 660 fb$^{-1}$ of data collected with the Belle detector at the KEKB asymmetric-energy $e^+e^-$ collider. We find no evidence for any of these decays. We obtain significantly improved upper limits on the branching fractions: $\mathcal{B}(D^0 \to \mu^+\mu^-) < 1.4 \times 10^{-7}$, $\mathcal{B}(D^0 \to e^+e^-) < 7.9 \times 10^{-8}$ and $\mathcal{B}(D^0 \to e^+\mu^-) + \mathcal{B}(D^0 \to \mu^+e^-) < 2.6 \times 10^{-7}$ at 90% confidence level.

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The flavor-changing neutral current (FCNC) decays $D^0 \to e^+e^-$ and $D^0 \to \mu^+\mu^-$ are highly suppressed in the standard model (SM) by the Glashow-Iliopoulos-Maiani mechanism [2]. With the inclusion of long distance contributions the branching fractions can reach values of around $10^{-13}$ [3]. The SM short distance Feynman diagrams for the $D^0 \to \mu^+\mu^-$ decay are shown in Fig. [1]. The lepton-flavor violating (LFV) decays $D^0 \to e^\pm\mu^\mp$ are forbidden in the SM, but are possible in extensions of the SM with nondegenerate neutrinos and nonzero neutrino mixings and are expected to be of the order of $10^{-14}$ [3] in these scenarios. All these predictions are orders of magnitude below the current experimental sensitivity.

FIG. 1. The SM short distance Feynman diagrams for the $D^0 \to \mu^+\mu^-$ decay.

In certain new physics (NP) scenarios, FCNC branching fractions can be enhanced by many orders of magnitude. For example, $R$-parity violating supersymmetry can increase the branching fractions of $D^0 \to e^+e^-$ and $D^0 \to \mu^+\mu^-$ up to $10^{-12}$ and $10^{-8}$, respectively [4]. The latter prediction is close to the current experimental sensitivity. As another example, so far unobserved leptoquarks were suggested as a possible explanation of the small discrepancy between the measured value of the $D_s$ meson decay constant and the prediction of lattice QCD [5]. Leptoquarks could also enhance the $D^0 \to \ell^+\ell^-$ branching fraction. In order to explain the measured $D^+_s \to \mu^+\nu$ width by a leptoquark contribution, and comply with other constraints arising from charm meson decays, $\mathcal{B}(D^0 \to \mu^+\mu^-)$ should be enhanced to $8 \times 10^{-7}$ [6]. The above examples demonstrate the importance of FCNC and LFV decays searches in the exploration of possible NP contributions. It should be noted that charm FCNC and LFV decays probe the couplings of the up-quark sector in contrast to $B$ or $K$ meson decays.

In this paper, we report on a search for the decays $D^0 \to \mu^+\mu^-$, $D^0 \to e^+e^-$ and $D^0 \to e^\pm\mu^\mp$ using 660 fb$^{-1}$ of data recorded in $e^+e^-$ collisions at the center-of-mass (CM) energy of the $\Upsilon(4S)$ resonance and 60 MeV below by the Belle detector at the KEKB collider.

The Belle detector, which is described in detail elsewhere [7], is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector (SVD) [8], a 50-layer central drift chamber (CDC), an array of aerogel Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter composed of CsI(Tl) crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside the coil is instrumented to detect $K_s^0$ mesons and to identify muons (KLM). Two inner detector configurations were used. A beam pipe with a radius of 2.0 cm and a 3-layer silicon vertex detector were used for the first sample of 155 fb$^{-1}$, while a 1.5 cm beampipe, a 4-layer silicon detector, and a small-cell inner drift chamber were used to record the remaining data sample.

In this measurement only $D^0$ mesons coming from $c$-quark production in the continuum $e^+e^- \to c\bar{c}$ process are considered. The inclusion of $D^0$ mesons from $B$ decays would result in a higher combinatorial background. We normalize the sensitivity of our search to topologically similar $D^0 \to \pi^+\pi^-$ decays; this cancels various systematic uncertainties. The $D^0 \to \ell^+\ell^-$ ($\ell = e$ or $\mu$) branching fraction is determined by

$$\mathcal{B}(D^0 \to \ell^+\ell^-) = N_{\ell\ell} f$$

where $N_{\ell\ell}$ is the number of reconstructed $D^0 \to \ell^+\ell^-$ decays and $f$ is defined as

$$f = \frac{1}{N_{\ell\ell}} \epsilon_{\ell\ell} \mathcal{B}(D^0 \to \pi^+\pi^-)$$

Here $\mathcal{B}(D^0 \to \pi^+\pi^-) = (1.397 \pm 0.027) \times 10^{-3}$ is the well-measured $D^0 \to \pi^+\pi^-$ branching fraction [9], $N_{\ell\ell}$ is the number of reconstructed $D^0 \to \pi^+\pi^-$ decays, and $\epsilon_{\ell\ell}$ and $\epsilon_{\pi\pi}$ are the reconstruction efficiencies for $D^0 \to \ell^+\ell^-$ and $D^0 \to \pi^+\pi^-$ decays, respectively.

The flavor-changing neutral current (FCNC) decays $D^0 \to e^+e^-$ and $D^0 \to \mu^+\mu^-$ are highly suppressed in the standard model (SM) by the Glashow-Iliopoulos-Maiani mechanism [2].
First, a general event selection is performed that is, apart from the particle identification criteria, the same for all data samples. Later in the analysis, tighter optimized criteria specific for each decay mode are used.

We use $D^0$ mesons from the decay $D^{*+} \rightarrow D^0 \pi^+_s$ with a characteristic low momentum pion, since this considerably improves the purity of the $D^0 \rightarrow \ell^+ \ell^-$ and $\pi^+ \pi^-$ samples. Each charged track is required to have at least two associated vertex detector hits in each of the two measurement coordinates. To select pion and lepton candidates, we impose standard particle identification criteria. Charged pions are identified using $dE/dx$ measurement from the CDC, Cherenkov light yields in the ACC, and timing information from the TOF. Muon identification is based on the matching quality and penetration depth of associated hits in the KLM. Electron identification is determined using the ratio of the energy deposit in the ECL to the momentum measured in the SVD and CDC, the shower shape in the ECL, the matching between the position of charged track trajectory and the cluster position in the ECL, the hit information from the ACC and the $dE/dx$ information in the CDC. The muon and electron identification efficiencies are around 90% with less than 1.5% and 0.3% pion misidentification, respectively, whereas the pion identification efficiency is around 83%. $D^0$ daughter tracks are refitted to a common vertex, and the $D^0$ production vertex is found by constraining the $D^0$ trajectory and the $\pi_s$ track to originate from the $e^+e^-$ interaction region; confidence levels exceeding $10^{-3}$ are required for both fits. A $D^{*+}$ momentum greater than 2.5 GeV/c in the CM frame of the collisions is required to reject $D$-mesons produced in B-meson decays and to suppress combinatorial background.

Candidate $D^0$ mesons are selected using two kinematical observables: the invariant mass of the $D^0$ decay products, $M$, and the energy released in the $D^{*+}$ decay, $q = (M_{D^{*+}} - M - m_\pi)^2$, where $M_{D^{*+}}$ is the invariant mass of the $D^0\pi_s$ combination and $m_\pi$ is the $\pi^+$ mass. We require $1.81 \text{ GeV}/c^2 < M < 1.91 \text{ GeV}/c^2$ and $q < 20 \text{ MeV}$.

According to Monte Carlo (MC) simulation based on EVTGEN and GEANT3, the background in $D^0 \rightarrow \ell^+ \ell^-$ decays originates predominantly from semileptonic B decays (80%) and from $D^0$ decays (10%). The background events can be grouped into two categories based on their $M$ distribution: (1) a smooth combinatorial background, and (2) a peaking background from the misidentification of $D^0 \rightarrow \pi^+ \pi^-$ decays. The decay $D^0 \rightarrow \pi^+ \pi^-$ contributes to the background when both pions are misidentified as muons or as a muon-electron combination. MC studies showed that misidentification of a K meson as a lepton does not produce a peak inside the mass region $1.81 \text{ GeV}/c^2 < M < 1.91 \text{ GeV}/c^2$.

The signal efficiencies $\epsilon_{\ell\ell}$ and $\epsilon_{\pi\pi}$ are evaluated using signal MC simulation, which is also based on EVTGEN and GEANT3, but includes final-state radiative effects (FSR) simulated by PHOTOS. Since we find differences between the widths of the $D^0 \rightarrow \pi^+ \pi^-$ signal in the data and MC simulation, we perform fits to the $M$ and $q$ distributions to obtain scaling factors for the signal widths, and then tune the shapes in the MC simulation by correcting $M$ and $q$ for each MC signal event by $M' = m_0 + (M - m_0) f_m$ and $q' = q_0 + (q - q_0) f_q$. Here, $m_0$ and $q_0$ denote the nominal $D^0$ mass and the nominal energy released in the $D^{*+}$ decay, respectively, and $f_m = 1.17$ and $f_q = 1.28$ are the corresponding scaling factors. Another difference, a small shift of $-0.2 \text{ GeV}$ in the mean of the distribution of the missing energy of the event ($E_{\text{miss}}$) between data and MC simulation is observed; we correct the MC distribution by subtracting, for every signal event, the above value from its $E_{\text{miss}}$.

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We construct $E_{\text{miss}}$ from the difference between the beam energy and the sum of the energies of all four vectors of photons and charged tracks, which are assumed to be pions. The constants derived from $D^0 \rightarrow \ell^+ \ell^-$ MC events are used to correct $D^0 \rightarrow \ell^+ \ell^-$ MC events. The uncertainties of the tuning procedure are included in the systematic error.

In order to avoid biases, a blind analysis technique has been adopted. All events inside the $D^0$ signal region of $|\Delta M| < 20 \text{ MeV}/c^2$ and $|\Delta q| < 1 \text{ MeV}$ were blinded until the final event selection criteria were established. Since $D^0 \rightarrow \ell^+ \ell^-$ decays are not expected to be observed at the current sensitivity, we optimize the selection criteria to obtain the best upper limits; we maximize the figure of merit, $F = \epsilon_{\ell\ell}/N_{UL}$, where $\epsilon_{\ell\ell}$ is the efficiency for detecting $D^0 \rightarrow \ell^+ \ell^-$ decays obtained from the tuned signal MC simulation and $N_{UL}$ is the Poisson average of Feldman-Cousins 90% confidence level upper limits on the number of observed signal events that would be obtained with the expected background and no signal.

The average upper limits $N_{UL}$ are calculated from the number of generic MC background events, surviving the selection criteria and scaled to the data size. The sample corresponds to 6-times the statistics of the data.

For the optimization we select the following variables: signal region size ($\Delta M, \Delta q$), $E_{\text{miss}}$, and minimal lepton identification probabilities. The quantities $\Delta M$ and $\Delta q$ are measured relative to the nominal $D^0$ mass and nominal energy released in the $D^{*+}$ decay, respectively. The signal region in $M$ is allowed to be asymmetric with respect to the nominal $D^0$ mass; for the $\mu\mu$ decay mode this provides some suppression of misidentified $D^0 \rightarrow \pi^+ \pi^-$ decays, since their invariant mass distribution peaks about 2 standard deviations below the $D^0$ mass; for the $ee$ and $e\mu$ modes an asymmetric requirement accounts for the low mass tail due to electron bremsstrahlung. The requirement on the maximal allowed missing energy in the event is chosen to suppress background from semileptonic $B$ decays; these events have larger missing energy due to undetected neutrinos. We found a broad maximum in $F$ for the lepton identification probability, hence we repeated the procedure at fixed lepton identification criteria, optimizing only the size of the signal region and the maximal allowed missing energy in an event. The results are summarized in Table I.
misidentification of weight each event by replacing the pion mass with the lepton mass and by the reconstructed \( D \) region determined by integration of the expected ratio of events in the signal and sideband region are summarized in Table II. The momentum \( p_D \) only to the \( D \) probabilities and efficiencies are measured in data using pion-lepton misidentification probability and pion identification is calculated as of combinatorial background events in the signal region are determined from a fit to the generic MC sample. The number of combinatorial background events in the signal region is calculated as \( N_{\text{bkg}} = p \times N_{\text{side}} \), where \( N_{\text{side}} \) is the number of events found in the sideband region and \( p \) is the expected ratio of events in the signal and sideband region determined by integration of \( f(M,q) \).

To estimate the number of combinatorial background events in the signal region, the sideband region \( |\Delta q| > 1 \) MeV is used. This region is chosen to reduce the statistical error and to exclude possible signal events and misidentifications. The comparison of data and MC simulation shows good agreement in the combinatorial background distribution in this region. The distribution is parametrized as \( f(M,q) = A(1 - BM)\sqrt{q} \), where the parameters \( A \) and \( B \) are determined from a fit to the generic MC sample. The number of combinatorial background events in the signal region is calculated as \( N_{\text{bkg}} = p \times N_{\text{side}} \), where \( N_{\text{side}} \) is the number of events found in the sideband region and \( p \) is the expected ratio of events in the signal and sideband region determined by integration of \( f(M,q) \).

The peaking background in the signal region due to misidentification of \( D^0 \rightarrow \pi^+\pi^- \) decays is estimated from the reconstructed \( D^0 \rightarrow \pi^+\pi^- \) decays found in data by replacing the pion mass with the lepton mass and by weighting each event by

\[
w = \frac{u(p_1, \cos \theta_1)u(p_2, \cos \theta_2)}{v(p_1, \cos \theta_1)v(p_2, \cos \theta_2)}
\]

where \( p_{1,2} \) and \( \theta_{1,2} \) are the momenta and polar angles of the outgoing pions and where \( u \) and \( v \) are the pion-lepton misidentification probability and pion identification efficiency, respectively. The misidentification probabilities and efficiencies are measured in data using \( D^+ \rightarrow D^0 \pi^+ \), \( D^0 \rightarrow K^-\pi^+ \) decays, binned in particle momentum \( p \) and cosine of polar angle.

The estimates for the number of background events in the signal region are summarized in Table I. The misidentification of \( D^0 \rightarrow \pi^+\pi^- \) contributes significantly only to the \( D^0 \rightarrow \mu^+\mu^- \) decay channel (1.8 events). The uncertainties in the background estimates listed in Table I include the statistical error on the number of sideband region events and the uncertainties in the combinatorial background parametrization, while the uncertainty in the peaking background estimation is negligible.

The invariant mass distributions after applying the optimized selection criteria are shown in Fig. 2. In the signal region we find two candidates in the \( D^0 \rightarrow \mu^+\mu^- \) mode, zero candidates in the \( D^0 \rightarrow e^+e^- \) mode, and three candidates in the \( D^0 \rightarrow e^+\mu^- \) mode; the yields are consistent with the estimated background.

A binned maximum likelihood fit is used to determine the yield of \( D^0 \rightarrow \pi^+\pi^- \) candidates for the normalization. We fit the invariant mass distribution using the same kinematic selections as for individual leptonic modes, except for the criteria on \( M \). The fit function is the sum of two Gaussian distributions with the same mean and an FSR tail for the signal, and a first-order polynomial for the background. The shape of the FSR tail and its relative normalization are taken from the corresponding signal MC simulation. The number of reconstructed \( D^0 \) mesons in the \( \pi^+\pi^- \) mode is found to be \( 51.2 \times 10^3 \), \( 44.1 \times 10^3 \), and \( 46.0 \times 10^3 \), using selection criteria for \( \mu\mu \), \( ee \), and \( e\mu \) modes, respectively. The invariant mass distribution of \( D^0 \rightarrow \pi^+\pi^- \) using the \( \mu\mu \) selection criteria with the fit curve superimposed is shown in Fig. 3. The relative uncertainties on \( N_{\pi\pi} \) are around 0.5%.

The signal efficiencies are determined from the tuned signal MC simulation. In addition, event weighting is applied to compensate for small differences in lepton and pion identification efficiencies between data and MC simulation. The correction factors for lepton identification were obtained using \( \gamma \gamma \rightarrow \ell^+\ell^- \) and \( B \rightarrow X J/\psi(\rightarrow \ell^+\ell^-) \) decays. The signal efficiencies are found to be between 5% and 7% for \( \ell^+\ell^- \) decays and about 11% for

| Mode   | \( \Delta M \) [MeV/c^2] | \( \Delta q \) [MeV] | \( E_{\text{miss}} \) [GeV] |
|--------|------------------------|-------------------|-------------------|
| \( \mu^+\mu^- \) | (−8, 19) | ±0.48 | 1.4 |
| \( e^+e^- \) | (−27, 14) | ±0.40 | 1.0 |
| \( e^+\mu^- \) | (−13, 15) | ±0.46 | 1.0 |

FIG. 2. The dilepton invariant mass distributions for (a) \( D^0 \rightarrow \mu^+\mu^- \), (b) \( D^0 \rightarrow e^+e^- \), and (c) \( D^0 \rightarrow e^+\mu^- \). The superimposed on the data (open histograms) are the estimated distribution for combinatorial background (filled histogram), the misidentification of \( D^0 \rightarrow \pi^+\pi^- \) (cross-hatched histogram), and the signal if the branching fractions were equal to the 90% confidence level upper limit (single hatched histogram).
The uncertainties in $\epsilon_{\ell\ell}$ are estimated to be 0.3% and include contributions from MC statistics (0.2%), lepton identification efficiency corrections (0.2%), and MC tuning (0.1%). The uncertainty in $\epsilon_{\pi\pi}$ is smaller (0.1%), because of a larger MC sample, better known pion efficiency corrections and a negligible contribution from MC tuning, since a wider range in $M$ is used.

From the number of reconstructed $D^0 \rightarrow \pi^+\pi^-$ decays, from the efficiency ratio, and from the known $D^0 \rightarrow \pi^+\pi^-$ branching fraction the factors $f$ are calculated with Eq. [2]. The relative uncertainties are around 5% (see Table II) and include the errors on $N_{\pi\pi}$, $\epsilon_{\ell\ell}$, $\epsilon_{\pi\pi}$ and the $D^0 \rightarrow \pi^+\pi^-$ branching fraction, summed in quadrature.

Finally, the branching fraction upper limits (UL) are calculated using the program pole.f [17], which extends the Feldman-Cousins method [16] by the inclusion of systematic uncertainties. We find that the inclusion of systematic uncertainties produces nearly the same result as the standard Feldman-Cousins method. The results are summarized in Table II. Note that $B (D^0 \rightarrow e^+\mu^-) + B (D^0 \rightarrow \mu^+e^-)$.

In summary, we have searched for the FCNC decays $D^0 \rightarrow \mu^+\mu^-$ and $D^0 \rightarrow e^+e^-$, and the LFV decays $D^0 \rightarrow e^+\mu^{\mp}$ using the Belle detector and have found no evidence of these decays. The upper limits on the branching fractions at the 90% confidence level are

$$B (D^0 \rightarrow \mu^+\mu^-) < 1.4 \times 10^{-7},$$
$$B (D^0 \rightarrow e^+e^-) < 7.9 \times 10^{-8},$$
$$B (D^0 \rightarrow e^+\mu^{\mp}) < 2.6 \times 10^{-7}.$$
Throughout this paper charge-conjugate modes are included.

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