Abstract

Motivation: Mathematical modelling of regulatory networks allows for the discovery of knowledge at the system level. However, existing modelling tools are often computation-heavy and do not offer intuitive ways to explore the model, to test hypotheses or to interpret the results biologically.

Results: We have developed a computational approach to contextualize logical models of regulatory networks with biological measurements based on a probabilistic description of rule-based interactions between the different molecules. Here, we propose a Matlab toolbox, FALCON, to automatically and efficiently build and contextualize networks, which includes a pipeline for conducting parameter analysis, knockouts and easy and fast model investigation. The contextualized models could then provide qualitative and quantitative information about the network and suggest hypotheses about biological processes.

Availability and implementation: FALCON is freely available for non-commercial users on GitHub under the GPLv3 licence. The toolbox, installation instructions, full documentation and test datasets are available at https://github.com/sysbiolux/FALCON. FALCON runs under Matlab (MathWorks) and requires the Optimization Toolbox.

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Supplementary information: Supplementary data are available at Bioinformatics online.
and are combinations of the fundamental ‘AND’, ‘OR’ and ‘NOT’ Boolean functions.

While Binary Boolean models (Kauffman, 1969) only consider full activation or complete absence, more quantitative approaches, for instance, Probabilistic Boolean Networks (PBNs) (Trairatphisan et al., 2013) and Dynamic Bayesian Networks (DBNs) (Lähdesmäki et al., 2006) can account for intermediate or continuous activation values and allow the integration of data uncertainty. These approaches are usually analyzed by Monte Carlo approaches (Mizer et al., 2016; Trairatphisan et al., 2014), which can be computationally demanding or non-intuitive to use. Here, we propose a tool called FALCON to efficiently contextualize logical regulatory networks based on steady-state experimental data. Our algorithm is based on DBNs and computes the expected value of the nodes by including an algebraic interpretation of the logical gates. The FALCON pipeline is shown in Figure 1.

2 Materials and methods
2.1 Modelling of logical networks
FALCON models biological regulatory systems as DBNs, which are directed graphical models defined by the set of $n$ nodes with $X = \{0, 1\}^n$ and the probability distribution $P(X_t|X_{t-1}) = \prod_{i=1}^n P(X^{(i)}_t|Pa(X^{(i)}_t))$ where $X^{(i)}_t$ denotes the $i$’th node at time $t$ and $Pa(X^{(i)}_t)$ represents the parents of $X^{(i)}_t$. These conditional probabilities are implicitly formulated by the structure of the network. The different nodes represent the different molecules of the system, with a value corresponding to the degree to which these molecules exist in their active form (for example, phosphorylated proteins). These node values can be understood as the proportion of the molecules in the system being active, or as the probability for a randomly chosen molecule to be active at time $t$.

In the FALCON framework, each molecular interaction is formulated as a logical predicate associated with a weight quantifying the relative importance of that specific interaction. We model different types of biochemical interactions with two types of edges: positive and negative edges connect activators and inhibitors to their downstream targets. Hyperedges corresponding to the ‘AND’ and ‘OR’ logical operations link multiple nodes to an output node, and model the activity of protein complexes and competition, respectively. Each edge and hyperedge is associated to a weight $k^{(i)}_j$ representing the relative influence of the upstream node to the downstream node. Because our modelling framework is grounded in Bayesian theory, the weights need to obey the law of total probability: for each node $X^{(i)}_t$ having a set $J_i$ of $m$ activating functions, we ensure the sum of activating weights $\sum_{j=1}^m k^{(i)}_j = 1$. Similarly, as weights of inhibiting interactions materialize the relative inhibition of upstream nodes, for nodes having a set $I_i$ of $l$ inhibiting functions, we ensure that $0 \leq \sum_{j=1}^l k^{(i)}_j \leq 1$.

Given a network structure established from prior knowledge, a set of parameters (weights) and a set of experimental conditions, the steady-state of the network is computed for each of the conditions and the values of the nodes corresponding to the measured species are recorded. For each one of the conditions, the nodes of the network are initialized with random values, except for the nodes considered as inputs (external to the system) for which the value is determined by the experimental condition and kept constant. The network is then updated repeatedly by computing synchronously for each node the expected value of its probability distribution, given the value of its parent nodes and the weights associated with each interaction.

$$X^{(i)}_t = \sum_{j=1}^m k^{(i)}_j Pa(X^{(j)}_t)^{J_i} \times \left( 1 - \sum_{j=1}^l k^{(i)}_j Pa(X^{(j)}_t)^{I_i} \right)$$

Because all nodes at each update are considered as independent, the inputs values of ‘AND’ logical gates are multiplied. The computation of ‘OR’ gates follows De Morgan’s law, i.e. the complement of the union of two sets is the same as the intersection of their complements. Inputs pointing to the same child node that are not members of a logical gate are summed. Table 1 summarizes the different types of interactions explicitly formulated in our framework. The algebraic formulas used for the computations can be directly derived.

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**Fig. 1.** The FALCON pipeline. Prior knowledge network and experimental data are combined to generate a network optimization problem. After the optimization process, the properties of the optimal network are then analyzed.
from the conditional probability tables of the DBN formulation of the logical interactions.

The resulting dynamical system converges to a steady-state where each node value corresponds to the normalized equilibrium concentration of the activated form of the molecule in the system.

2.2 Contextualization algorithm

Objective function. To perform the contextualization of the model with experimental data, we extract from the network at steady-state the value of the nodes corresponding to the measurements, compare them with the normalized values from the experimental data and compute the mean squared error (MSE) between the estimated values and the measurements. We minimize this measure of the error by optimizing the value of the weights using a gradient-descent algorithm. To guarantee high efficiency while allowing for arbitrary degrees of recurrence in the networks, we use the interior-point method (Waltz et al., 2004). A scheme of the FALCON workflow is presented in Figure 1.

Rapid optimization. Using the gradient-descent optimization algorithm fmincon with interior-point method, FALCON is able to rapidly estimate the set of weights that minimizes the objective function. Random initialization of the weights is done either from a uniform distribution across the [0, 1] range, or from a truncated normal distribution centred on 0.5, depending on users’ choice. Normally distributed initial values have been shown to improve learning for deep neural networks (Glorot and Bengio, 2010) and in our hands, increase the speed of convergence of the optimization algorithm.

2.3 Subsequent analyses on optimized logical networks

Once a set of parameters has been inferred from a given topology and dataset, a series of additional analyses can be performed to gain more insight into the systems-level properties of the regulatory network being modelled as summarized in Figure 2.

Robustness of optimized parameter values. Depending on the topology of the network, the uncertainty in the measurement of some nodes can have more impact on the parameter values of the model than others. FALCON can analyze the uncertainty on inferred parameter values by sampling a user-defined number of artificial datasets based on original experimental measurements and determining the weights of the model in the light of the new data (Fig. 2a). The artificial datasets are constructed from the average experimental measurements and their associated error, assuming normally distributed residuals.

Identifiability analysis. In order to assess the identifiability of the model parameters, an approach similar to Raue et al. is applied (Raue et al., 2009). For each parameter, the algorithm samples the range of possible parameter values [0, 1], and re-optimizes the model under the additional constraint of this parameter being fixed to each of the sampled values. In order to obtain the most meaningful results we sample the same number of points on both sides of the optimal value. We include the option to skip the most extreme values based on a threshold determined by the resampling analysis (red line, Fig. 2b), thereby accelerating computations. The resulting MSE profiles allow to determine which parameters are well constrained by the experimental measurements.

Interactions knockouts. FALCON allows the systematic removal of each edge in the network and provides a graphical output showing the effect on the global fitness of the model. The models are compared using the Akaike Information Criterion (Burnham and Anderson, 2004), which balances goodness-of-fit with model complexity (Fig. 2c). By using this additional analysis, it is possible to differentiate the crucial edges of the system from the ones that are dispensable, which can be pruned out.

Nodes knockouts. A frequent goal of systems biology analyses is to identify the crucial molecules of a regulatory network. Often performed via network topological properties (centrality measures), this identification is of particular interest in the case of target discovery efforts. FALCON allows the systematic evaluation of models in which each node is removed from the network. The comparison of these models using the Akaike Information Criterion allows to identify these crucial nodes not only from topological properties but from the effect their removal has on the behaviour of the entire system (Fig. 2d).

Differential regulation. In many real-life modelling applications, a system is studied in different contexts. For example, during a drug screen, the same signalling pathways are studied for different cell lines, or over time. One goal of systems biology is to identify differences between the contexts in the way the system is regulated. FALCON automates such analyses by optimizing identical models in parallel for multiple series of experimental conditions. Users can discover which parts of the network are activated or shut down between cell lines/time points, and this may lead to the identification of specific interventions strategies for each context (Fig. 3).

3 Pipeline and performance

FALCON is a highly efficient optimization tool that is capable of contextualizing small-to-large biological networks. For an easy input of model structure and experimental data, FALCON accepts different file formats (.txt, .xls, .xlsx, .csv) which are subsequently used to build the model structure and experimental data, FALCON accepts different file formats (.txt, .xls, .xlsx, .csv) which are subsequently used to build logical models. Inference of network structure, interaction matrices and parameter constraints are fully automated, and the toolbox outputs a user-friendly summary comprising the optimized weights for the different interactions, both in text and graphical forms. To facilitate the use of our toolbox, we included a graphical user interface (GUI) to guide users through the different steps of the workflow. Users who are more comfortable with the MATLAB language can instead choose to use the provided driver script for full flexibility.

To showcase the performance of our toolbox, we provide four examples, including the replication of several studies, each presenting a particular challenge for the toolbox. The results of our tests are shown in Table 2. All computations were performed on a
desktop PC with 16 GB RAM and an Intel® Xeon® CPU E3-1246 v3, 3.5 GHz with Matlab 2016b.

**Toy model:** we demonstrate the basic functionality of FALCON on a 6-node toy model, comprising both positive and negative interactions, as well as a Boolean AND gate. The structure of this network, associated synthetic data and trained model are illustrated in Supplementary Figure S1.

**PDGF:** we used FALCON to optimize a platelet-derived growth factor signalling model (Trairatphisan et al., 2016), comprising 30 nodes and 37 interactions (19 free parameters). The dataset was

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**Fig. 2.** Analyses of optimized model in FALCON (PDGF model). (a) Parameter robustness analysis; red stars: optimal parameter values, blue bars: standard deviations of parameter values fitting to 10 resampling datasets. (b) Parameter identifiability analysis of parameter ‘km3’ from panel a; Red line: threshold used to speed up computations in the ‘fast’ mode. (c) Interaction knock-out analysis. (d) Node knock-out analysis. In panels c and d, the color of the bars indicates the sign of the difference with the base model (blue). Green indicate better models (AICmodel < AICbase), black indicates worse ones. Abbreviations: MSE = mean squared error, AIC = Akaike Information Criterion

**Fig. 3.** Differential analyses in FALCON. The same prior knowledge model is contextualized in parallel with different datasets corresponding to different contexts. Subsequent analysis can identify context-specific parametrizations and topologies.
Table 2. Accuracy and computation times for the different examples

| Example  | Nodes Edges/Parameters | Datapoints | Cost | Speed |
|----------|------------------------|------------|------|-------|
| Toy (artificial) | 6 3/3 | 10 0 | < 1 s | |
| PDGF     | 30 19/19 | 36 | 0.004 1.3 s | |
| Apoptosis | 138 160/41 | 18 | 0.017 76 s | |
| MAPK [FALCON] | 22 32/32 | 175 | 0.036 1.1 s | |
| MAPK [CNORfuzzy] | 22 32/92 | 175 | 0.032 47.4 s | |

Note: The cost is expressed as MSE (mean squared error) and the speed is expressed in seconds (s).

assembled from the quantification of 6 proteins by western blot analysis in HEK293 cells expressing a constitutively active form of the PDGF receptor, in the presence or absence of two types of perturbations: single-point mutations of tyrosine residues on the PDGF receptor associated with the recruitment sites of downstream signalling molecules, and kinase inhibitors. We obtained a fitting cost (MSE = 0.0041) and parameter values very similar to the original study, where the tool optPBN (Trairatphisan et al., 2014) was used to perform the optimization, and in accordance with it, we are able to train the network with single perturbations and accurately predict the signalling profiles of combined perturbations experiments (see Supplementary Material).

Apoptosis: we replicated a modified model of a previous study in which a large Boolean model of apoptosis was used to investigate non-linear dose-effects of UV radiation on cultured hepatocytes (Schlatter et al., 2009; Trairatphisan et al., 2014). The model comprises 138 nodes and 160 interactions (41 free parameters). We correctly estimated apoptosis levels and the other associated experimental measures, and could draw the same conclusions as the original study concerning the importance of cross-talks, especially between Caspase 8 and NFkB (see Supplementary Material). While the original study used the software CellNetAnalyzer (Klamt et al., 2007), which uses a multi-value Boolean formalism and concentrates on network properties, a previous replication with the optPBN tool (Trairatphisan et al., 2014) could infer more quantitative properties, but at the expense of long computation times. Analysis of this network and data with FALCON is comparatively very fast with up to 170-fold improvement (FALCON: 76 seconds; optPBN: 4 hours 40 minutes) and we obtained a fitting cost (FALCON: MSE = 0.017) comparable with the previous studies (optPBN: MSE = 0.011; Schlatter et al.: MSE = 0.013). In comparison, CellNetAnalyzer, using discrete Boolean modelling and only able to consider either full activation of complete inactivity of the molecules, achieves a worse fit (MSE: 0.056). The comparison of the inferred molecular states of optPBN and FALCON can be found in Supplementary Figure S6.

MAPK: we compared the performance of our tool with the software CellNOptR (MacNamara et al., 2012; Terfve et al., 2012) in the fuzzy logic mode (CNORfuzzy) for quantitative optimization of model states. Using the toy example provided, which is the optimized network of the DREAM4 challenge and contains 22 nodes, 36 interactions and 25 experimental conditions (Pripp et al., 2011), we obtained a similar fitting cost with FALCON (MSE = 0.036) and with CellNOptR (MSE = 0.032) but with a gain of speed of about 44 times (see Table 2).

4 Discussion
We present FALCON as an alternative tool for the efficient optimization and comprehensive analysis of logical models of regulatory networks. Our modelling framework, based on DBNs, is able to determine qualitative and quantitative features of the systems being modelled. Node values, being comprised in the interval [0, 1], represent the probabilities for molecules to be in their active state at equilibrium. They can also be understood as the normalized average activities of the nodes. The computed parameters, or weights, also comprised in the interval [0, 1] and subject to the law of total probability, represent the probabilities for the designated interactions to influence downstream nodes. They can also be interpreted as the relative influences of the parent nodes on their children nodes and are useful in assessing the flow of the signal transduction.

FALCON, through its GUI, is easy to use for scientists without extensive modelling experience. FALCON is also very fast compared to similar tools based on PBNs, and surpassed CellNOptR in our test. The low computation costs make it possible to analyze the models at the systems level through a series of bundled additional analyses which allow to answer a number of biologically important questions: whether the parameter values are well constrained by the available data, how the experimental error influences the confidence in the parameter values, and which are the nodes and interactions most crucial to the behaviour of the system versus the ones that can be pruned out. Together, our results suggest that FALCON is a very useful software for rapid model exploration, especially for large networks and large datasets.

Compared to the popular package CellNOptR, the FALCON pipeline is faster in contextualizing a small graphical model with quantitative data. The inferred parameters are also more intuitively understandable as the relative strength of the interactions, while CellNOptR combines linear and Hill’s equations in a way that does not encourage direct interpretation. This relative complex formulation, together with the multiple concurrent formalisms proposed and the increased computational cost suggest reserving this tool for more complex tasks, while FALCON is better adapted for exploratory studies of larger networks and datasets.

Future development of the FALCON toolbox will include full compatibility with established model representation formats (SBML-Qual, Bio-PAX), and the conversion of the toolbox to other languages, like R, Python and C++. One particular aspect that we regard as highly interesting is the use of FALCON to explore model topologies in a large-scale, systematic way to uncover previously unknown mechanisms in regulatory networks.

In terms of applications, we demonstrated that FALCON is applicable to model signal transduction networks and could easily be extended to study other biological regulatory systems. We envision that FALCON has the potential to be widely adopted by the computational biology community, including biologists with limited programming experience.

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