Orbital selectivity in Hund’s metals: The iron chalcogenides

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We show that electron correlations lead to a bad metallic state in chalcogenides FeSe and FeTe despite the intermediate value of the Hubbard repulsion $U$ and Hund’s rule coupling $J$. The evolution of the quasiparticle weight $Z$ as a function of the interaction terms reveals a clear crossover at $U \simeq 2.5$ eV. In the weak coupling limit $Z$ decreases for all correlated $d$ orbitals as a function of $U$ and beyond the crossover coupling they become weakly dependent on $U$ while strongly dependent on $J$. A marked orbital dependence of the $Z$’s emerges even if in general the orbital-selective Mott transition only occurs for relatively large values of $U$. This two-stage reduction of the quasiparticle coherence due to the combined effect of Hubbard $U$ and the Hund’s $J$ suggests that the iron-based superconductors can be referred to as Hund’s correlated metals.

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I. INTRODUCTION

The role of electron correlations in the iron-based superconductors is still a debated issue, naturally intertwined with the search for the origin of high critical temperatures. We present results that improve the qualitative understanding of how electron correlation influences fundamental electron properties of these compounds, such as the metallicity, which in turn might be important also for the understanding of the pairing mechanism. We choose two candidates of the chalcogenides, FeSe and FeTe, and employ first principles electron structure calculations combined with advanced many-body methods taking into account the local electron correlation. The chalcogenides have a simpler atomic structure with respect to the pnictides; thus they are easier to study theoretically. In addition, they are nontoxic in contrast to the pnictides containing arsenic.

In previously known superconductors we can identify either weakly correlated materials, like elemental superconductors or binary alloys, including MgB$_2$, or highly correlated compounds like the copper oxides and heavy fermion materials. In the first set of compounds superconductivity is explained within the Bardeen-Cooper-Schrieffer framework and its extensions, and it occurs as a pairing instability of a normal metal. In the second set it is widely believed that correlations revolutionize the electronic properties and that both the metallic state and the pairing mechanism deviate from standard paradigms.

The iron-based pnictides and chalcogenides superconductors do not fit this simple classification. The common labeling “intermediate correlation,” referring to properties such as Fermi surface topology or absence of Hubbard bands, suggests modest effects of correlations. Conversely, the metallic state appears much less coherent than what these observations imply. A magnetic counterpart of this dualism is the localized and itinerant nature of the spin-density-wave state of the parent compound.

The characteristic property of the band structure is that several of the five $d$ bands cross the Fermi level. The multiorbital nature leads to several exotic electronic properties such as orbital selectivity and also to the conclusion that the interorbital exchange or Hund’s coupling plays a key role.

The role of the Hund’s coupling has indeed been recognized in the early stages of the field in a dynamical mean-field theory (DMFT) study by Haule and Kotliar, who coined the definition of Hund’s metals by the observation that the quasiparticle effective mass and the response functions are much more sensitive to the Hund’s coupling $J$ than to the Hubbard $U$ interaction.

For a Hund’s metal the spectral weight is not transferred to the high-energy Hubbard bands, but rather spreads over a scale controlled by $J$. Other DMFT studies have highlighted the anomalies of the metallic state, showing its incoherent nature and its relation with a spin-freezing crossover. In Ref. 16 the dual nature of the magnetic correlation is shown to induce a remarkable difference between a large instantaneous magnetic moment and smaller long-time magnetic correlations, similar to the spin-freezing scenario proposed in Ref. 17 for a three-orbital model.

It has recently been shown that $J$ can have a twofold effect on a multiorbital system with an integer filling different from one electron per orbital, a situation which is realized in the parent compounds of iron superconductors, in which six electrons populate the five $d$ orbitals. In this configuration $J$ reduces the quasiparticle coherence temperature (or coherence energy scale), while it increases the critical $U$ for the Mott transition.

As a consequence, a two-stage reduction of the electronic coherence scale (measured by the quasiparticle weight $Z$) occurs as a function of $U$. Indeed, if we choose a sizable value of $J$ and follow the evolution of the metallic properties, we first have a rapid decrease of the effective Fermi-liquid coherence scale, which leads to a bad metal already for intermediate correlations strengths, while the Mott transition occurs only at much larger $U$. This opens a window of $U$ in which $Z$ is essentially flat, which has been dubbed after the roman
god Janus in view of the double-faced effect of the Hund’s coupling.18

II. METHOD

In this work we explore the combined role of $U$ and $J$ in the iron-based chalcogenides FeSe and FeTe by means of the Gutzwiller approximation (GA). The GA is a simplified treatment of electron correlations which systematically selects the energetically favorable electronic configurations out of an uncorrelated wave function. The method provides a reasonable description of the Mott transition from the metallic side19 and allows for a numerically cheap investigation of a wide range of model parameters.

We employ the GA numerical scheme developed in Refs. 20–22, which is a generalization of earlier formulations of the GA method23–26 and which enables taking into account the full rotationally invariant Hund’s terms, including the so-called spin-flip and pair-hopping, that are often hard to treat with approximate analytical methods and even with numerical methods. Since the formation of a Hund’s metal is actually associated with a differentiation between the different atomic multiplets, we expect that the GA will perform even better than for standard Mott transitions.

Based on electronic structure calculations of FeSe and FeTe combined with the GA we show that the electronic configuration of the parent compounds of iron-based superconductors form an ideal system with a two-stage reduction of electronic coherence. Furthermore, the bad metal arising from the interplay of $U$ and $J$ displays, as expected, an orbital-selective coherence with $t_{2g}$ orbitals significantly more correlated than $e_g$.

The material-specific band structure is determined using density functional theory with the generalized gradient approximation for the exchange-correlation potential according to the Perdew-Burke-Ernzerhof recipe as implemented in Quantum Espresso.27 Then we apply WANNIER9028 to compute the maximally localized Wannier orbitals, and we include the interaction terms of the form

$$H = U \sum_{i,m} n_{i m \uparrow} n_{i m \downarrow} + \left(U' - \frac{J}{2}\right) \sum_{i,m,m'} n_{i m} n_{i m'} - J \sum_{i,m,m'} [2 S_{i m \uparrow} S_{i m' \downarrow} + (d_{i m \uparrow}^\dagger d_{i m' \downarrow}^\dagger + H.c.)].$$

(1)

Here $d_{i m \sigma}$ is the destruction operator of an electron of spin $\sigma$ at site $i$ in orbital $m$, and $n_{i m \sigma} \equiv d_{i m \sigma}^\dagger d_{i m \sigma}$, $n_{i m} \equiv \Sigma_{\sigma} d_{i m \sigma}^\dagger d_{i m \sigma}$, and $S_{i m \sigma}$ is the spin operator for orbital $m$ at site $i$. $U$ and $U' = U - 2J$ are intra- and interorbital repulsions and $J$ is the Hund’s coupling. The values of $U$ and $J$ are not directly accessible from experiments and, even if reliable theoretical estimates are obtained with constrained random-phase approximation, there are still some discrepancies between different calculations. In the light of the extreme sensitivity on the value of the parameter $J$, it is particularly useful to apply a method such as the present GA which allows for a continuous sweep of many parameter values.

III. NUMERICAL CALCULATIONS

As mentioned above, one of the distinctive features of the iron-based superconductors is that all five $d$ orbitals appear to contribute to the band structure around the Fermi level. As a first step we consider a system with five degenerate $d$ bands, and show that the configuration with six electrons per atom, characteristic of the parent compounds, is a clear-cut case of a “Janus” scenario, characterized by a two-stage reduction of the quasiparticle weight.

In Refs. 11 and 18 it is clearly shown that the two-stage reduction of the electronic coherence scale is a consequence of a contrasting effect of $J$ on the metallic character of the electrons. In the weak-coupling limit $J$ favors the formation of a large local magnetic moment, which leads to a faster decay of the electronic coherence scale $Z$, while in the strong coupling the Mott transition is pushed to larger $U$. This effect is particularly strong when the number of electrons per atom differs by one unit from the number of orbitals $N = N_{\text{orb}} \pm 1$, and it is expected to be emphasized increasing the number of orbitals as the weak-coupling coherence temperature scales exponentially with $N_{\text{orb}}$.

A. Physical insight from models

In Fig. 1 we compare the GA results for the two cases of $N = N_{\text{orb}} \pm 1$ when $N_{\text{orb}} = 5$ and $N_{\text{orb}} = 3$. We clearly see that the former case has a much clearer separation between the different atomic multiplets, and a strongly two-faced correlation physics, we move towards the realistic situation in order to identify how the material-specific
properties influence this picture. As an intermediate step, we lift the degeneracy with a cubic crystal field which is present in iron pnictides and chalcogenides. An energy splitting \( \Delta \) is introduced between the three \( t_{2g} \) and the two \( e_g \) orbitals. In Fig. 2 we show the results for \( \Delta/D = 0.2 \). We observe that, while the weak-coupling region gives an essentially orbital-independent \( Z \), as soon as we enter in the strongly correlated region, the low-lying states become more correlated than the higher lying. In other words, the crystal-field triggers a strongly orbital-selective renormalization in the bad metal state.

**B. First principle study: The iron chalcogenides**

We finally perform the realistic DFT + GA calculation for iron chalcogenides. In panel (a) of Fig. 3 we show the evolution of the quasiparticle weight for the different orbitals as a function of \( U \), keeping the ratio \( J/U \) fixed to 0.224. This ratio is chosen according to the estimates presented in Ref. 29 for FeSe. The picture remains similar to the idealized systems. For small values of \( U \) the \( Z \)’s for the different orbitals are similar and they appreciably decrease as a function of \( U \) before \( U \approx 2.5 \text{ eV} \), where the system enters the novel regime in which the \( Z \)’s are small and almost constant as a function of \( U \). However, an orbital dependence also appears clearly. In addition to the differentiation of the \( t_{2g} \) and \( e_g \) orbitals, we find that the \( d_{xy} \) orbital is the most correlated and the \( d_{z^2-r^2} \) is more localized than the \( d_{3z^2-r^2} \). The crossover, which roughly separates a weakly correlated phase from a bad metallic phase, takes place at a value of \( U \) smaller than the bandwidth \( 2D \) (\( \approx 4 \text{ eV} \)), and much smaller than the multiband Mott transition, which would take place at a \( U \) of the order of five times the width of each band.\(^{30}\)

It is easy to see that in the atomic limit the ground state changes from low spin (\( S = 1 \)) to high spin (\( S = 2 \)) when \( J \) becomes larger than the crystal-field splittings (\( \approx 0.6 \text{ eV} \) for FeSe). In the metallic phase this evolution yields a crossover to a \( S = 2 \) state [panel (b)] which leads to the rapid reduction of \( Z \).\(^{11}\)

**FIG. 2.** (Color online) Upper panel: quasiparticle weight in a Hubbard model with six electrons in five bands with semicircular densities with half-bandwidth \( D \) split by a cubic crystal field in two manifolds of degeneracy 3 (\( t_{2g} \) symmetry) and 2 (\( e_g \) symmetry). Lower panel: populations of the two manifolds.

**FIG. 3.** (Color online) Results for FeSe (DFT + GA with \( J/U = 0.224 \)) as a function of \( U \). From the top: (a) the quasiparticle weights for the different orbitals; (b) the expectation value of \( S^2 \); (c) the renormalized crystal-field splittings; (d) the population of each orbital; (e) the interorbital density correlations.

This crossover leads to a dramatic lowering of the coherence temperature, and opens a wide bad-metal region due to the increase of \( U_c \) induced by the effect of \( J \) on the high-spin Mott gap. This behavior is observed even more pronounced in studies of LaFeAsO\(^{31}\) and the intercalated chalcogenides.\(^{32}\) It contributes in a substantial manner to the sharp onset of the Hund’s metal\(^{19}/\)spin-frozen\(^{15}/\)incoherent\(^{13,14}\) phase observed in all DMFT studies.

This effect is also reflected in the renormalized orbital energies [panel (c) of Fig. 3], with four of the five orbitals being brought close to one another and also near the Fermi level by the interactions. This favors a more even population of the orbitals that gains in exchange energy, and favors the high-spin configurations over the low-spin ones. The evolution of the population of the different orbitals is shown in panel (d) of Fig. 3. The \( t_{2g} \) orbitals have populations closer to half-filling already at the DFT level, while the \( e_g \) bands are more occupied. Increasing the interaction the \( d_{xy} \) level, which has the smaller \( Z \), becomes less occupied than \( d_{xz} \) and \( d_{yz} \) due to the stronger effect of correlations. Analogously,
the large difference between the noninteracting densities of the two $e_g$ bands is washed out by correlations, which favor a more democratic occupation with high spin. The same low to high spin transition within the metallic phase occurs for any sizable value of $J$ and it is indeed present already in the model with a simple $t_{2g}$-$e_g$ splitting as clear from the nonmonotonic population behavior shown in the lower panel of Fig. 2.

In panel (e) of Fig. 3 we show the interorbital density correlation functions, which are clearly suppressed in the correlated regime. This suppression, driven by $J$, has been put forth\(^{4,30}\) as the driving mechanism behind the orbital selectivity. Indeed $J$ acts as an “orbital decoupler” (“band decoupler,”\(^{30}\) for weak orbital hybridization) suppressing interorbital charge fluctuations, and rendering the charge dynamics of each orbital virtually independent. For a smaller value of $J/U$, 0.15, the picture does not change (see Fig. 4). The position of the crossover is only weakly affected, while the values of the $Z$’s in the bad metallic region after the crossover depend strongly on $J$. The behavior observed confirms previous findings of a $Z$ which depends strongly on $J$ and weakly on $U$ in the physically relevant region of $U \sim 4$ eV and $J \sim 0.5$–1 eV. At the same time our results clearly underline that such a “Hund’s metal” requires a critical value of the Hubbard repulsion, albeit much smaller than one might expect on the basis of the value of the bandwidth. The picture is clearly consistent with that drawn in Ref. 18. Finally, we show the quasiparticle weights for FeTe using the same value of the interaction coefficients.

FIG. 4. (Color online) Results for FeSe and smaller $J/U = 0.15$ (top panel) and for FeTe (bottom panel).

In summary, we have calculated the correlation strength induced by many-body correlations on the \textit{ab initio} electronic structure of the iron chalcogenides FeSe and FeTe. We find, in agreement with previous analogous studies on LaFeAsO\(^{31}\) and K\(_{1-x}\)Fe\(_x\)Se\(_2,32\) that Hund’s coupling has a strong influence on the electronic properties of the paramagnetic phase, inducing a two-stage quasiparticle renormalization. A first regime at weak coupling sees a moderate correlation affecting all orbitals comparably. After a quick decrease around $U \simeq 2.5$ eV, a value much smaller than the overall bandwidth, a strongly correlated regime is entered, heavily differentiated among the orbitals (with $t_{2g}$ orbitals sensibly more correlated), in which the quasiparticle weights are almost independent of $U$. The Mott transition occurs at much higher ($\sim 5$ times the bandwidth) interaction strengths. Comparison with idealized models shows that the two-staged reduction of the quasiparticle weights is due to the filling of six electrons in five bands, thus placing the system in the “Janus” regime induced by Hund’s coupling,\(^{13}\) and that, by introducing a crystal-field $t_{2g}$-$e_g$ splitting, orbital differentiation happens once entered in the Janus regime, where the orbitals closest to half-filling are more correlated.\(^{30}\) This is an example of the orbital-decoupling action of Hund’s coupling, a mechanism\(^{4,30}\) occurring also in simple metallic iron,\(^{33}\) and recently seen to apply generally to iron superconductors and to be enhanced, in particular, by hole doping.\(^{34}\) Another, different, source of orbital differentiation in the magnetic phases of pnictides was individuated in the spin-orbit coupling.\(^{35}\)

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\begin{thebibliography}{99}
\bibitem{1} W. L. Yang \textit{et al.}, Phys. Rev. B \textbf{80}, 014508 (2009).
\bibitem{2} G. R. Stewart, Rev. Mod. Phys. \textbf{83}, 1589 (2011).
\bibitem{3} D. C. Johnston, Adv. Phys. \textbf{59}, 803 (2010).
\bibitem{4} L. de’ Medici, S. R. Hassan, M. Capone, and X. Dai, Phys. Rev. Lett. \textbf{102}, 126401 (2009).
\bibitem{5} L. de’ Medici, S. R. Hassan, and M. Capone, J. Supercond. N. Magn. \textbf{22}, 535 (2009).
\bibitem{6} S. P. Kou, T. Li, and Z. Y. Weng, Europhys. Lett. \textbf{88}, 17010 (2009).
\bibitem{7} A. Hackl and M. Vojta, New J. Phys. \textbf{11}, 055064 (2009).
\bibitem{8} W.-G. Yin, C.-C. Lee, and W. Ku, Phys. Rev. Lett. \textbf{105}, 107004 (2010).
\bibitem{9} E. Bascones, B. Valenzuela, and M. Calderon, arXiv:1208.1917.
\bibitem{10} K. Haule and G. Kotliar, New J. Phys. \textbf{11}, 025021 (2009).
\bibitem{11} A. Georges, L. de’ Medici, and J. Mravlje, arXiv:1207.3033.
\bibitem{12} Z. P. Yin, K. Haule, and G. Kotliar, Nat. Mater. \textbf{10}, 932 (2011).
\bibitem{13} H. Ishida and A. Liebsch, Phys. Rev. B \textbf{81}, 054513 (2010).
\bibitem{14} A. Liebsch and H. Ishida, Phys. Rev. B \textbf{82}, 155106 (2010).
\end{thebibliography}
15 P. Werner, M. Casula, T. Miyake, F. Aryasetiawan, A. J. Millis, and S. Biermann, Nature Phys. 8, 331 (2012).
16 P. Hansmann, R. Arita, A. Toschi, S. Sakai, G. Sangiovanni, and K. Held, Phys. Rev. Lett. 104, 197002 (2010).
17 P. Werner, E. Gull, M. Troyer, and A. J. Millis, Phys. Rev. Lett. 101, 166405 (2008).
18 L. de’ Medici, J. Mravlje, and A. Georges, Phys. Rev. Lett. 107, 256401 (2011).
19 W. F. Brinkman and T. M. Rice, Phys. Rev. B 2, 4302 (1970).
20 N. Lanatà, H. U. R. Strand, X. Dai, and B. Hellsing, Phys. Rev. B 85, 035133 (2012).
21 N. Lanatà, Y. Yao, and G. Kotliar (unpublished).
22 H. U. R. Strand, N. Lanatà, M. Granath, and B. Hellsing (unpublished).
23 M. Fabrizio, Phys. Rev. B 76, 165110 (2007).
24 N. Lanatà, P. Barone, and M. Fabrizio, Phys. Rev. B 78, 155127 (2008).
25 N. Lanatà, P. Barone, and M. Fabrizio, Phys. Rev. B 80, 224524 (2009).
26 X. Y. Deng, L. Wang, X. Dai, and Z. Fang, Phys. Rev. B 79, 075114 (2009).
27 P. Giannozzi et al., J. Phys.: Condens. Matter 21, 395502 (2009).
28 A. A. Mostofi, J. R. Yates, Y.-S. Lee, I. Souza, D. Vanderbilt, and N. Marzari, Comput. Phys. Commun. 178, 685 (2008).
29 M. Aichhorn, S. Biermann, T. Miyake, A. Georges, and M. Imada, Phys. Rev. B 82, 064504 (2010).
30 L. de’ Medici, Phys. Rev. B 83, 205112 (2011).
31 R. Yu and Q. Si, Phys. Rev. B 86, 085104 (2012).
32 R. Yu and Q. Si, arXiv:1208.5547.
33 A. A. Katanin, A. I. Poteryaev, A. V. Efremov, A. O. Shorikov, S. L. Skornyakov, M. A. Korotin, and V. I. Anisimov, Phys. Rev. B 81, 045117 (2010).
34 L. de’ Medici, G. Giovannetti, and M. Capone, arXiv:1212.3966.
35 J. Wu, P. Phillips, and A. H. Castro Neto, Phys. Rev. Lett. 101, 126401 (2008).