Multifunctional antiferromagnetic materials with giant piezomagnetism and noncollinear spin current

Hai-Yang Ma1,5, Mengli Hu2,5, Nana Li2,5, Jianpeng Liu2, Wang Yao3, Jin-Feng Jia1,4✉ & Junwei Liu2✉

We propose a new type of spin-valley locking (SVL), named C-paired SVL, in antiferromagnetic systems, which directly connects the spin/valley space with the real space, and hence enables both static and dynamical controls of spin and valley to realize a multifunctional antiferromagnetic material. The new emergent quantum degree of freedom in the C-paired SVL is comprised of spin-polarized valleys related by a crystal symmetry instead of the time-reversal symmetry. Thus, both spin and valley can be accessed by simply breaking the corresponding crystal symmetry. Typically, one can use a strain field to induce a large net valley polarization/magnetization and use a charge current to generate a large noncollinear spin current. We predict the realization of the C-paired SVL in monolayer V2Se2O, which indeed exhibits giant piezomagnetism and can generate a large transverse spin current. Our findings provide unprecedented opportunities to integrate various controls of spin and valley with nonvolatile information storage in a single material, which is highly desirable for versatile fundamental research and device applications.
Exploring new quantum degrees of freedom (DOFs) and finding new control approaches are crucial to realize multifunctional materials for developing the next-generation information technologies. For instance, the periodicity in a crystal can endow degenerate but inequivalent valleys in the electron dispersion, forming an emergent DOF that can encode information as spin. Moreover, spin and valley DOFs can be further locked together to form the spin-valley locking (SVL) as proposed in transition metal dichalcogenides owing to the strong spin-orbital coupling and the time-reversal symmetry. SVL enables many dynamical control approaches and dramatically increases the depolarization time for both spin and valley, as spin flipping needs to change valley index and vice versa. However, it is very difficult to realize information storage (memory) in these SVL materials since the information is encoded by the spin and valley of carrier or current.

The discoveries of graphene and other 2D materials provide excellent material platforms to study these emergent quantum DOFs and their control approaches at the microscopic level. Being atomically thin, 2D materials are easier to engineer via gate modulation, strain, and proximity effect. Recent discoveries of atomic-thin ferromagnetic and antiferromagnetic (AFM) materials further enriched the 2D material family and opened a new era for spintronics and valleytronics with nonvolatile magnetic information storage. Moreover, 2D AFM materials possess many other desirable features such as higher-speed operation and lower-energy consumption as proposed in the AFM spintronics.

In this work, by coupling the valley DOF to the AFM order in a single material, we propose a new type of SVL, named C-paired SVL, which can simultaneously realize giant piezomagnetism and large noncollinear spin current, thus enabling both static and dynamical controls of spin and valley, one usually needs to create heterostructures of SVL and 2D magnetic materials. In monolayer VO$_2$. In addition, due to the weak or absence of SOC and protection of SVL as in conventional SVL systems, long spin depolarization time can be expected, which is critical for spintronics applications.

Compared with the conventional SVL and CuMnAs-type AFM materials, the C-paired SVL material can realize multiple functions in one single material and possesses advantages of different systems and many other unique properties. Typically, one can use both static AFM order and the spin/valley of carriers/current to encode and process information. The former one gives rise to nonvolatile memory, and the latter one provides many other dynamic approaches as optical methods in conventional SVL materials. Moreover, both static and dynamic information can be naturally transformed to each other in C-paired SVL materials since a spin current can affect the AFM order and vice versa. In addition, the magnetoelastic coupling intrinsically exists in C-paired SVL materials, which enables the direct conversion between magnetic and mechanical properties, realizing many unique phenomena like piezomagnetism and magnetostrictive and making C-paired SVL materials very useful in various sensors.

Our findings provide a new class of multifunctional material platform that combines versatile static and dynamic controls of spin and valley with high-density nonvolatile information storage, and extend these studies into more general systems of no or weak SOC and collinear AFM systems, which opens up a variety of opportunities for finding more suitable materials in device applications of spintronics and valleytronics.

### General theory of C-paired SVL and its unique properties

Valley in a crystal refers to the degenerate energy extrema well separated in momentum space, and its strong coupling to the unzoned spin realizes the SVL. As shown in Fig. 1a, for the conventional SVL in transition metal dichalcogenides, strong SOC makes both spin and valley states very different, making the spin-orbit coupling (SOC) essential. If there is no SOC, the valley splitting is much reduced, and vice versa. In this case, we refer to this type of SVL as SOC-free SVL.

In C-paired SVL, spin-orbit coupling (SOC) is no longer a necessary condition and the valley-contrasted spin splitting can arise from strong exchange coupling of itinerant electrons to AFM order and hence can be as large as several eVs. Moreover, valley splitting in C-paired SVL systems also depend on the crystal symmetries at bilayer TMDs and strained MoS$_2$.

We first show that one can also realize SVL in an AFM system even without SOC. As shown in Fig. 1b, the AFM order breaks the time-reversal symmetry and generally induces a spin splitting between states $\Psi_0^+$ and $\Psi_0^-$ through strong exchange couplings, i.e., $E^\uparrow \neq E^\downarrow$ if there is no PT symmetry. One can prove that there must be another two spin-polarized states $\Psi_{C-K}$ and $\Psi_{C-K}$ but with switched energy $E^\uparrow \neq E^\downarrow$ at the crystal-symmetry-related valley $K \leftarrow C \leftarrow K$, i.e., $H_K \Psi_{C-K}^\uparrow = E^\uparrow \Psi_{C-K}^\downarrow$ and $H_K \Psi_{C-K}^\downarrow = E^\downarrow \Psi_{C-K}^\uparrow$, where $C$ is the crystal symmetry connecting the two AFM sublattices.

Dynamical controls of spin and valley DOFs. We predict its materialization in monolayer VO$_2$. In addition, due to the weak or absence of SOC and protection of SVL as in conventional SVL systems, long spin depolarization time can be expected, which is critical for spintronics applications.

Different valleys in C-paired SVL form an emergent quantum DOF, which can be used to encode information as spin. Moreover, they are related by a crystal symmetry instead of the time-reversal symmetry as in $T$-paired SVL. Thus, one can use various approaches like a strain or electric field to break the crystal symmetry to access this quantum DOF easily, which will give rise to many interesting phenomena and applications like...
One typical result (De40, the leading effect of a strain on the band edge of a 2D gapped system) is from strong spin-orbit coupling (SOC) when inversion symmetry is broken, and the two valleys are related by the time-reversal (T) symmetry. Using the deformation potential tensor \( \mathbf{D} \), which relates the strain to the polarization, upon finite doping with carrier density \( n \), there will be a net static magnetization \( M = \int_{-\infty}^{E_f} [\rho^+(e) - \rho^-(e)] \, de \), where \( E_f \) is the Fermi level and \( \rho^+ \) and \( \rho^- \) are the spin-up and spin-down density of states and can be assumed as a constant \( \rho \) around the band edge of a 2D gapped system. The strain-induced magnetization is then obtained as

\[
M(\theta, \epsilon_\theta, n) = \begin{cases} 
-\gamma \sin(2\phi - 2\theta) \epsilon_\theta, & 0 \leq \epsilon_\theta < \frac{n}{|\gamma \sin(2\phi - 2\theta)|} \\
-\text{sign}(\gamma \sin(2\phi - 2\theta)) n, & \epsilon_\theta \geq \frac{n}{|\gamma \sin(2\phi - 2\theta)|}
\end{cases}
\]

(1)

giant piezomagnetism and noncollinear spin current. In general, various crystal symmetries can lead to the C-paired SVL, and to make discussions concrete we will focus on the mirror symmetry in the following parts.

As shown in Fig. 1b, there are two valleys related by a mirror symmetry \( M_x \) where \( \phi \) is the angle between the mirror plane and the \( x \) axis (defined as the main axis of the valley with spin-up polarization), and a strain can easily break the mirror symmetry to induce a valley polarization. Using the deformation potential theory, the leading effect of a strain on the band edge of a gapped system is to shift the energy by \( \text{Tr}(D\epsilon) \), where \( \epsilon \) is the strain tensor and \( D \) is the deformation potential tensor. By using \( D' = M_x D M_x^{-1} \), we can get the strain-induced energy difference between the two valleys as \( \delta E = [(D_{xx} - D_{yy}) \sin^2 2\phi - D_{xy} \sin 4\phi] (\epsilon_{xx} - \epsilon_{yy}) + [4D_{xy} \cos^2 2\phi (D_{xx} - D_{yy}) \sin 4\phi] \epsilon_{xy} \). Considering a uniaxial strain \( \epsilon_\theta \) along \( \theta \) direction, the energy shift is \( \delta E = [(D_{xx} - D_{yy}) \sin 2\phi - 2D_{xy} \cos 2\phi] \sin(2\phi - 2\theta) \epsilon_\theta \) (more details in Sec. 1B of SI). Since different valleys have opposite spin polarization, upon finite doping with carrier density \( n \), there will be a net static magnetization \( M = \int_{-\infty}^{E_f} [\rho^+(e) - \rho^-(e)] \, de \), where \( E_f \) is the Fermi level and \( \rho^+ \) and \( \rho^- \) are the spin-up and spin-down density of states and can be assumed as a constant \( \rho \) around the band edge of a 2D gapped system. The strain-induced magnetization is then obtained as

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\end{cases}
\]

(1)

where \( \gamma = \rho((D_{xx} - D_{yy}) \sin 2\phi - 2D_{xy} \cos 2\phi) \) is a constant depending on the details of the materials. As shown in Fig. 1c, the magnetization linearly increases with strain until all the carriers are fully polarized at a fixed doping. In addition, the magnetization depends on the strain direction with a periodicity of \( \pi \). Piezomagnetism is the strongest for \( \theta = \phi \pm \pi/4 \) and is zero for \( \theta = \phi \) or \( \phi \pm \pi/2 \), which is consistent with the symmetry analysis because a normal strain in or perpendicular to the mirror plane does not break the mirror symmetry. Moreover, the magnetization here is not because of the realignment of local magnetic moments as in conventional piezomagnetism, but from strain-induced occupation imbalance between spin-up and spin-down electrons, which is mainly determined by electronic density of states.
property anisotropy and could be very large to realize a giant piezomagnetism. Note that, $T$-paired SVL systems can also realize a net magnetization through breaking the time-reversal symmetry as using a charge current in strained MoS$_2$\cite{38}, whereas it is dynamic properties and disappears once the charge current is switched off. On the contrary, in $C$-paired SVL system, it is a static property owing to piezomagnetism arisen from the intrinsic magnetoelastic coupling. This coupling can also lead to magnetostriction where one can induce a strain using an external magnetic field. All these properties make $C$-paired SVL materials good candidates for magnetic sensors and applications in other fields\cite{42}.

Besides a static strain field, a charge current under an electric field can also dynamically induce the imbalance between the two valleys in $C$-paired SVL, and spontaneously generate a noncollinear spin current from the anisotropy of valleys with different spins. Around the band edge of a gapped system, the dispersion can be generally approximated as $E(k) = \frac{k^2}{2m_1} + \frac{k^2}{2m_2}$, where $m_1$ and $m_2$ are the effective mass. Based on the Boltzmann equation and mirror symmetry $M_s$, the spin conductivity under an electric field along $\theta$ direction (Fig. 1d) can be calculated as

$$
\sigma^{\lambda} = \sigma^K - \sigma^K' = 4\sigma_0^a \left( -\sin(2\phi - 2\theta) \cos(2\phi - 2\theta) \right)
$$

where $\sigma^K$ and $\sigma^K'$ are the conductivity contributed from different valleys and $\sigma_0^a = ne^2 \tau \frac{(m_1 - m_2)}{m_1 m_2} \sin 2\phi$ is a parameter depending on the materials with carrier density $n$ and relaxation time $\tau$ (more details in Sec. IC of SI). The most remarkable property is that there will always be a spin current with a constant magnitude $|\sigma^a_0 E|_\theta$ independent of the electric field direction. In detail, the direction of spin current indeed depends on the electric field direction $\theta$, and the most interesting case is $\theta = \pm \pi$ (i.e., electric field is in the mirror plane, see Fig. 1d). The charge current will be along the electric field direction, whereas the spin current will be perpendicular to the charge current, similar to the spin Hall effect\cite{33}, i.e., a spin current appears in the direction perpendicular to the charge current\cite{30}. Different from in the spin Hall effect from strong SOC or noncollinear magnetic order, the transverse spin current in $C$-paired SVL originates from the anisotropic responses of valleys to the external electric field owing to different effective mass along different directions, and the equivalent spin Hall angle is $\Delta S_{\phi} = \frac{(m_1 - m_2)\tan 2\phi}{m_1 + m_2 - (m_1 - m_2)\cos 2\theta}$ which is determined by the effective mass anisotropy and thus can be very large. At last, it is worth emphasizing that owing to SVL and the absence of SOC, the depolarization time of the spin current can be very long. Thus, an AFM material of $C$-paired SVL can serve as an ideal device to generate pure spin current, which is highly desirable in AFM spintronics\cite{27-30}.

$C$-paired SVL in monolayer $V_2Se_2O$. Based on symmetry analysis and first-principles calculations, we find that the proposed $C$-paired SVL can be realized in monolayer $V_2Se_2O$, which we predict to be a 2D AFM material based on the crystal field theory, extensive first-principles calculations, the general Goodenough–Kanamori–Anderson rules\cite{43-45}, and model Hamiltonian analysis.

The existence of $C$-paired SVL in monolayer $V_2Se_2O$ is rooted in its crystal symmetries. As shown in Fig. 2a, monolayer $V_2Se_2O$...
has a tetragonal structure consisting of three atomic layers with two V atoms and one O atom in the middle layer sandwiched by two Se-atom layers. Each V atom is surrounded by four Se and two O atoms as a distorted octahedron, possessing a local magnetic moment around 2 µB, and the two V-atom sublattices form the 2D Neél AFM order (Fig. 2b). Moreover, these two sublattices are related by a mirror symmetry with respect to Se-O-Se plane (Fig. 2a) but cannot be transformed to each other by any translation operation, which, together with the AFM order, frees spin DOF and hence enables the C-paired SVL even without SOC.

The detailed band structures are calculated by DFT+/U methods and verified by hybrid functional methods (see Methods and Fig. S15–16), and the results are shown in Fig. 2c. There are two valleys at X and Y points related by the mirror symmetry (Fig. 2d). States around X and Y points are mainly from V1 and V2 atom, respectively (Fig. S17–185) and indeed have opposite spins due to the Neél AFM order, which leads to the C-paired SVL in the absence of SOC. Even considering SOC, the form of SVL is unchanged, as enforced by the mirror symmetry (more details in Fig. S19).

The bulk V2Se2O has VdW layered crystal structure and has been synthesized in experiments recently, and the monolayer V2Se2O is thermal-dynamically stable (Fig. S23). Moreover, the cleavage energy of the bulk and in-plane stiffness of monolayer V2Se2O is calculated to be comparable to graphite and graphene, which indicates that monolayer V2Se2O can be easily exfoliated from the bulk (Fig. S23). Very recently, bulk V2Te2O has also been synthesized. Although they have the same crystal structure, their electronic and magnetic properties are completely different. V2Se2O is insulating and has large local magnetic moments, whereas V2Te2O is metallic with no local magnetic moments. Based on our systematic calculations and analysis, these differences can be attributed to the different crystal field effect, which is stronger in V2Se2O owing to the larger electronic negativity of Se and shorter V-Se bonds. Moreover, the large crystal field effect in V2Se2O also leads to stronger exchange interactions between local magnetic moments (~85 meV), which forces local magnetic moments to form the in-plane AFM alignment as shown in Fig. 2. With such an in-plane AFM alignment, bulk V2Se2O is a semiconductor independent of the out-of-plane magnetic orders (Fig. S6–7), whereas V2Te2O is always metallic even we assume it has the same magnetic structure (Fig. S9). Although the strong in-plane AFM ordering, bulk V2Se2O only exhibits paramagnetic behavior, which is owing to the small interlayer coupling (~0.11 meV) and in-plane magnetic anisotropy (~0.05 meV). All these theoretical results are consistent with and explain well experimental observations. Thus, we can conclude that monolayer V2Se2O can have the AFM order even bulk V2Se2O is paramagnetic, as the similar scenario for VSe2, whose monolayer is strong room-temperature ferromagnetic, whereas the bulk is paramagnetic. In addition, owing to very strong in-plane AFM interaction, one can use an external magnetic field to further stabilize the AFM order if the magnetic anisotropy turns out to be too small as for monolayer NiPS2. More details about the AFM order in monolayer V2Se2O can be found in Sec. II and Sec. III of SI.

Besides the conventional methods, one can also use spin-polarized scanning tunneling microscope/spectroscopy (STM/STS) to measure the magnetic structure directly in real space to the AFM order in monolayer V2Se2O. Moreover, the SVL offers another more-convenient approach of simply using quasi-particle interference (QPI) as implemented in an ordinary STM. For an ordinary semiconductor, both the inter-valley scattering (q1 and q2) and intra-valley scattering (q1 and q2) can happen, and QPI patterns will exist around both the center and the corner like Fig. 2e. However, due to the C-paired SVL, the opposite spin of different valleys will strongly suppress the inter-valley scattering (q1 and q2), and QPI patterns will be only around the center but not the corner like Fig. 2f, i.e., the AFM order here can be easily confirmed by the absence of scatter patterns around the corner in QPI image. In addition to STM, one can use angle-resolved photoemission spectroscopy (ARPES) to measure the band structure and even use spin-resolved ARPES to directly measure the C-paired SVL.

Piezomagnetism in monolayer V2Se2O. As proposed above, the C-paired SVL can easily generate a valley polarization using a strain and may realize a giant piezomagnetism. As shown in Fig. 3a and S20, a compressive/tensile strain along a direction makes the energy of X valley E(X) lower/higher than that of Y valley E(Y), and the valley polarization P = E(X) – E(Y) depends on the strain monotonously (Fig. 3b). Meanwhile, the strain along b direction generates exactly the opposite valley polarization since two valleys are related by a diagonal mirror symmetry (Fig. 3b).

To determine the magnetization upon finite doping accurately, we carefully tested the convergence of k grids using various methods (more details in Sec. IIIG). Without loss of generality, we focus on hole doping. As shown in Fig. 3c, the magnetization increases with both carrier density and strain, and the magnetization direction is indeed opposite for tensile and compressive strains. The typical quantitative dependence is shown in Fig. 3d. Same as the general theory, the magnetization linearly depends on the strain in a small strain region, and eventually saturates for very large strains, where all the carriers are polarized and hence the magnetization is always equal to the number of holes per unit cell. The piezomagnetic coefficient between magnetization and strain has some dependence on the carrier density, as the effective mass is no longer a constant when considering the high order effect of strain (Fig. S21). Similar results but with opposite magnetization direction happen when the strain is along b direction since C-paired SVL here is enabled by the diagonal mirror symmetry (Fig. S22). Compared with piezomagnetism in noncollinear magnetic materials, piezomagnetism here is much larger, and the magnetization direction can be tuned using various methods since the AFM order is collinear and magnetic anisotropy energy is very small (~10–2 meV). So far, monolayer V2Se2O is the first 2D material, which can realize the piezomagnetism.

Noncollinear spin current generation in monolayer V2Se2O. As shown in Fig. 2d, valleys of monolayer V2Se2O are highly anisotropic, which suggests a giant noncollinear spin current generation as analyzed above. Without SOC, spin is a good quantum number and the conductivity of spin-up and spin-down electrons (σ↑↓) can be well defined and calculated. As shown in Fig. 4a, for electric field along x direction, only the longitudinal current exists, and σ0↑ is always smaller than σ0↑ for the Fermi level in [–2, 2] eV, and the spin current is also along x direction with the spin conductivity σ0↑ = σ0↑ – σ0↓. To study the angle dependency of the spin current quantitatively, we choose Fermi level to be ~0.2 eV. As shown in Fig. 4b, both the longitudinal and transverse conductivity σ↑↑ and σ↑↓ oscillate with the electric field direction θ with a period of π, and can be well characterized by

\[ \sigma^{\uparrow \downarrow}(\theta) = \sigma_0 \pm \sigma_0 \cos 2\theta \]

and

\[ \sigma^{\uparrow \downarrow}(\theta) = \sigma_0 \pm \sigma_0 \cos 2\theta \]
saturates. Compressive and tensile strains in the region of small strains. When strain is large enough, all the carriers are polarized, and the net magnetization is almost a constant that depends on the strain. The magnetization for different hole densities.

Strain induced valley polarization, which destrains along

Fig. 3 Strain induced valley polarization and piezomagnetism in hole doped monolayer V$_2$Se$_2$O. a, Band structure evolution under different uniaxial strains along a direction (−5%, 0%, and −5%). Compared with the energy $E(X)$ at X valley, the energy $E(Y)$ at Y valley monotonously shifts down. b, Strain induced valley polarization, which defined as the energy difference between two valleys $P = E(X) - E(Y)$. c, Diagram of strained induce net magnetization for different hole densities. d, For a given hole density, the net magnetization increases linearly with strain but has an opposite direction for compressive and tensile strains in the region of small strains. When strain is large enough, all the carriers are polarized, and the net magnetization saturates. e, For any given strain, the magnetization is always equal to the number of holes per unit cell when the doping is light. However, for heavy doping, the magnetization is almost a constant that depends on the strain.

$\sigma^i_\uparrow\downarrow(\theta) = \mp \sigma^i_\downarrow\uparrow(\theta)$ sin2θ. The longitudinal and transverse spin conductivity can be easily obtained as $\sigma^i_\uparrow\downarrow(\theta) = \sigma^i_\downarrow\uparrow(\theta) = -2 \alpha \delta \cos 2\theta$ and $\sigma^i_\downarrow\uparrow(\theta) = \sigma^i_\uparrow\downarrow(\theta) = 2 \alpha \delta \sin 2\theta$ (Fig. 4c). Same as the general theory, the noncollinear spin current is a constant independent of the electric field direction. As shown in Fig. 4d, the directions of both charge current and spin current depend on the electric field direction. Although there are transverse charge currents from individual valleys, while they cancel with each other and hence the charge current is always along the electric field direction $\theta$. However, the spin currents from two valleys cannot cancel, resulting in a net spin current in the direction $\pi - \theta$ (Fig. 4d), linear in the electric field strength. Moreover, when $\theta = \pi/4$ and $\theta = 3\pi/4$, the spin current will be perpendicular to the charge current (and electric field), and the equivalent spin Hall angle is 0.7, much larger than the reported values due to SOC.

The spin splitting here (> 1 eV as shown in Fig. 3c and S16c) is also much larger than in the T-paired SVL, together with the absence of or very weak SOC, a long depolarization time of spin current can be very long, which is critical for the spintronics applications.

Besides 2D AFM materials, C-paired SVL can generally exist in 3D AFM materials. Based on symmetry analysis and first-principles calculations, we found C-paired SVL can also exist in the following experimentally verified AFM materials, NaOsO$_3$, LaMnO$_3$, LaCrO$_3$, TbFeO$_3$, MnTe, RuO$_2$, MnF$_2$, FeF$_2$, CoF$_2$, and NiF$_2$. Owing to the complexity of 3D magnetic space groups and band structures, we will put detailed studies of these materials in another work. In addition, a complete search of C-paired materials could be done using the high-throughput method in future work.

In conclusion, we proposed a new type of SVL, C-paired SVL, which has many advantages like giant piezomagnetism and noncollinear spin current. Via first-principles calculations, we predicted that monolayer V$_2$Se$_2$O, whose bulk compound has been synthesized recently, can host the C-paired SVL, which is also the first 2D piezomagnetic material under doping. In view of experimental studies, the angle-dependent spin current can be measured with standard schemes, the 2D Néel magnetic structure in real space can be visualized by spin-polarized STM/STS, and the C-paired SVL in momentum space can be directly detected using spin-resolved ARPES or QPI as implemented in STM. External strain can be induced by depositing V$_2$Se$_2$O on a substrate with moderate lattice mismatch such as (001) surface of MgO (4.21 Å).

Methods

The calculations are performed in the framework of density functional theory as implemented in Vienna ab initio simulation package. The projector-augmented wave potential is adopted with the plane-wave energy cutoff set at 600 eV. The exchange-correlation functional of the Perdew–Burke–Ernzerhof type has been used for both structural relaxations and self-consistent electronic calculations. The GGA+U method is employed to treat the strong correlations of the V 3d orbitals, where the value of the Hubbard $U$ is taken as 5.1 eV, and the Hund’s rule coupling $J$ is taken as 0.8 eV. These two interaction parameters are determined by fitting the band structure obtained from the hybrid functional calculations. The Brillouin zone is sampled by a $9 \times 9 \times 1$ gamma-centered Monkhorst–Pack mesh, and the convergence criteria for the electronic iteration are set to $10^{-6}$ eV. Denser $k$
mesh has been very carefully tested to give converged results in the calculations of piezomagnetism and conductivity.

Data availability
The authors declare that the data supporting the findings of this study are available within the article and the corresponding Supporting Information file. All other relevant source data are available from the corresponding author upon reasonable request.

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References
1. Rycerz, A., Twozydlo, J. & Beenakker, C. W. J. Valley filter and valley valve in graphene. Nat. Phys. 3, 172–175 (2007).
2. Xiao, D., Yao, W. & Niu, Q. Valley-contrasting physics in graphene: magnetic moment and topological transport. Phys. Rev. Lett. 99, 236809 (2007).
3. Xiao, D. et al. Coupled spin and valley physics in monolayers of MoS2 and other group-VI dichalcogenides. Phys. Rev. Lett. 108, 196802 (2012).
4. Mak, K. F., He, K., Shan, J. & Heinz, T. F. Control of valley polarization in monolayer MoS2 by optical helicity. Nat. Nanotechnol. 7, 494–498 (2012).
5. Yang, L. et al. Long-lived nanosecond spin relaxation and spin coherence of electrons in monolayer MoS2 and WS2. Nat. Phys. 11, 830–834 (2015).
6. Schubley, J. R. et al. Valleytronics in 2D materials. Nat. Rev. Mater. 1, 16055 (2016).
7. Mak, K. F. & Shan, J. Photonics and optoelectronics of 2D semiconductor transition metal dichalcogenides. Nat. Photonics 10, 343–350 (2014).
8. Castro Neto, A. H., Guinea, F., Peres, N. M. R., Novoselov, K. S. & Geim, A. K. The electronic properties of graphene. Rev. Mod. Phys. 81, 109–162 (2009).
9. Novoselov, K. S., Mishchenko, A., Carvalho, A. & Castro Neto, A. H. 2D materials and van der Waals heterostructures. Science 353, 461 (2016).
10. Song, J. C. W. & Gabor, N. M. Electron quantum metamaterials in van der Waals heterostructures. Nat. Nanotechnol. 13, 986–993 (2018).
11. Novoselov, K. S. et al. Electric field effect in atomically thin carbon films. Science 306, 666–669 (2004).
12. Li, J. et al. A valley valve and electron beam splitter. Science 362, 1149–1152 (2018).
13. Feng, J., Qian, X., Huang, C. W. & Li, J. Strain-engineered artificial atom as a broad-spectrum solar energy funnel. Nat. Photonics 6, 866–872 (2012).
14. Avsar, A. et al. Spin-orbit proximity effect in graphene. Nat. Commun. 5, 4875 (2014).
15. Gong, C. et al. Discovery of intrinsic ferromagnetism in two-dimensional van der Waals crystals. Nature 546, 265–269 (2017).
16. Huang, B. et al. Layer-dependent ferromagnetism in a van der Waals crystal down to the monolayer limit. Nature 546, 270–273 (2017).
17. Deng, Y. et al. Gate-tunable room-temperature ferromagnetism in two-dimensional Fe3GeTe2. Nature 563, 94–99 (2018).
19. Bonilla, M. et al. Strong roomerature ferromagnetism in VSe2 monolayers on van der Waals substrates. Nat. Nanotechnol. 13, 289–293 (2018).
20. Fei, Z. et al. Two-dimensional itinerant ferromagnetism in atomically thin Fe3GeTe2. Nat. Mater. 17, 778–782 (2018).
21. Wang, X. et al. Raman spectroscopy of atomically thin two-dimensional magnetic iron phosphorus trisulfide (FeP3S3) crystals. 2D Mater. 3, 031009 (2016).
22. Suenaga, K. et al. Ising-type magnetic ordering in atomically thin FeP3S3. Nano Lett. 16, 7433–7438 (2016).
23. Cai, X. et al. Atomically thin CrCl3: an in-plane layered antiferromagnetic insulator. Nano Lett. 19, 3993–3998 (2019).
24. Kim, K. et al. Suppression of magnetic ordering in XXZ-type antiferromagnetic monolayer NiP3S3. Nat. Commun. 10, 345 (2019).
25. Cai, X. et al. Direct observation of van der Waals layered antiferromagnetic metal. Sci. Adv. 6, eaay6407 (2020).
26. Lei, S. et al. High mobility in a van der Waals layered antiferromagnetic metal. Sci. Adv. 6, eabf2522 (2020).
27. Jungwirth, T. et al. The multiple directions of antiferromagnetic spintronics. Nat. Phys. 14, 200–203 (2018).
28. Balz, V. et al. Antiferromagnetic spintronics. Rev. Mod. Phys. 90, 15005 (2018).
29. Šmejkal, L., Mokrousov, Y., Yan, B. & MacDonald, A. H. Topological antiferromagnetic spintronics. Nat. Phys. 14, 242–251 (2018).
30. Železny, J., Wadley, P., Olejnik, K., Hoffmann, A. & Ohno, H. Spin transport and spin torque in antiferromagnetic devices. Nat. Phys. 14, 220–228 (2018).
31. Wadley, P. et al. Electrical switching of an antiferromagnet. Science 351, 587–590 (2016).
32. Zhong, D. et al. Van der Waals engineering of ferromagnetic semiconductor heterostructures for spin and valleytronics. Sci. Adv. 3, e1603113 (2017).
33. Sinova, J., Valenzuela, S. O., Wunderlich, J., Back, C. H. & Jungwirth, T. Spin freedom to antiferromagnetic order. Proc. Natl. Acad. Sci. 110, 3738–3742 (2013).
34. Li, X., Cao, T., Niu, Q., Shi, J. & Feng, J. Coupling the valley degree of freedom to antiferromagnetic order. Proc. Natl. Acad. Sci. 110, 7893–7897 (2013).
35. Jiang, S., Xie, H., Shen, J. & Mak, K. F. Exchange magnetostriction in two-dimensional antiferromagnets. Nat. Mater. 19, 1295–1299 (2020).
36. Wu, S. et al. Electrical tuning of valley magnetic moment through symmetry control in bilayer MoS2. Nat. Phys. 9, 149–153 (2013).
37. Lee, J., Mak, K. F. & Shen, J. Electrical control of the valley Hall effect in bilayer MoS2 transistors. Nat. Nanotechnol. 11, 421–426 (2016).
38. Lee, J., Wang, Z., Xie, H., Mak, K. F. & Shen, J. Valley magnetoelectricity in single-layer MoS2. Nat. Mater. 16, 887–891 (2017).
39. Li, X., Cao, T., Niu, Q., Shi, J. & Feng, J. Coupling the valley degree of freedom to antiferromagnetic order. Proc. Natl. Acad. Sci. 110, 7893–7897 (2013).
40. Sun, Y., Thompson, S. E. & Nishida, T. Strain Effect in Semiconductors: Theory and Device Applications. Springer (Springer, 2009). https://doi.org/10.1007/978-1-4419-0532-4_4.
41. Jaime, M. et al. Piezomagnetism and magnetoelectric memory in uranium dioxide. Nat. Commun. 8, 99 (2017).
42. Eerenstein, W., Mathur, N. D. & Scott, J. F. Multiferroic and magnetoelectric materials. Nature 442, 759–765 (2006).
43. Goodenough, B. An interpretation of the magnetic properties of the perovskite-type mixed crystals. J. Phys. Chem. Solids 6, 287–297 (1958).
44. Kanamori, J. Superspin interaction of electron and symmetry. J. Phys. Chem. Solids 10, 87–98 (1959).
45. Anderson, P. W. & Hasegawa, H. Considerations on double exchange. Phys. Rev. 100, 675–681 (1955).
46. Lin, H. et al. Structure and physical properties of CaVs2Se2-xO and V2Se2O. Phys. Rev. B 98, 075132 (2018).
47. Abkhit, A. et al. V2Te2O: a two-dimensional van der waals correlated metal. Inorg. Chem. 57, 14617–14623 (2018).
48. Joy, P. A. & Vasudevan, S. Magnetism in the layered transition-metal thiophosphates MFS3 (M=Mn, Fe, and Ni). Phys. Rev. B 46, 5425–5434 (1992).
49. Pai, C. F. et al. Spin transfer torque devices utilizing the giant spin Hall effect of tungsten. Appl. Phys. Lett. 101, 122404 (2012).
50. Liu, L. et al. Spin-torque switching with the giant spin Hall effect of tantalum. Science 336, 555–558 (2012).
51. Kreine, G. & Forthmüller, J. Efficiency of ab initio total energy calculations for metals and semiconductors using a plane wave basis set. Comput. Mat. Sci. 6, 15 (1996).
52. Vanderbilt, D. Soft self-consistent pseudopotentials in a generalized eigenvalue formalism. Phys. Rev. B 41, 7892–7895 (1990).
53. Liechtenstein, A. I., Anisimov, V. I. & Zaanen, J. Density-functional theory and strong interactions: orbital ordering in Mott-Hubbard insulators. Phys. Rev. B 52, 5467–5471 (1995).
54. Heyd, J., Scuseria, G. E. & Ernzerhof, M. Erratum: hybrid functionals based on a screened coulomb potential. J. Chem. Phys. 124, 2005–2006 (2006).

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Author contributions
H. Ma, M. Hu, and N. Li contributed equally to this work. J. Liu initiated the work and conceived the idea. J. Liu and J. Jia supervised the work. All the authors discussed the results and contributed to the manuscript.

Competing interests
The authors declare no competing interests.

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Correspondence and requests for materials should be addressed to J.-F.J. or J.L.

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