Comparison of methods for estimation of genetic covariance matrix from SNP or pedigree data utilised to predict breeding value

Sebastian Mucha*, Anna Wolc, Tomasz Strabel

From 13th European workshop on QTL mapping and marker assisted selection
Wageningen, The Netherlands. 20-21 April 2009

Abstract

Background: The aim was to predict breeding values of non-phenotyped individuals based on a dataset prepared for the 13th QTL-MAS Workshop in Wageningen.

Methods: Genetic co-variance matrices between animals were estimated with three methods: one using pedigree information only and two based on SNP markers from the first chromosome. Quadratic regression of breeding values, estimated separately in each of the five time points, was used to predict the breeding values in the 6th time point.

Results: Based on the comparison (true - estimated BV) it can be concluded that SNP based methods provided better estimates (accuracy between 0.75 and 0.80) than pedigree (0.65).

Conclusions: Even though only SNPs from chromosome 1 were used it was still possible to achieve fairly high accuracies. Most likely this was due to the fact that chromosome 1 contained the QTLs with the largest effects.

Background

The analysis was based on a dataset prepared for the 13th QTL-MAS Workshop in Wageningen [1]. The aim of this paper was to predict breeding values of the 1000 non-phenotyped animals in the 6th time point, using three different strategies based on similarity between individuals due to common ancestry (pedigree records), and two methods based on marker similarity. Due to software limitations [2] only one chromosome could be included in the analysis. The first chromosome was chosen based on preliminary results of QTL mapping, performed with a single QTL model with additive effects in the GRID QTL package [3]. The most significant QTLs, affecting the analysed trait in all five time points, were found on chromosome 1.

Methods

Estimation of genetic relationship

Genetic covariance matrices between all animals present in the dataset were estimated with three methods. First approach (pedigree based method - PB) was based on the additive relationship matrix calculated from pedigree. Second method computed similarity between individuals as a correlation coefficient between allelic states using 90 SNP markers from chromosome 1 (SNP based method - SNPL). For this purpose the method of Loi-selle [4] was used as implemented in software package SPAGeDi 1.2g [2], which computes relationship as $a_{ij} = \frac{\sum a(c_1, \Sigma c_1(x_{1cia} - p_{1a})(x_{1cia} - p_{1a}))}{\sum a(p_{1a}(1 - p_{1a}))}$ where $x_{1cia}$ is an indicator variable ($x_{1cia} = 1$ if the allele on chromosome $c$ at locus $l$ for individual $i$ is $a$, otherwise $x_{1cia} = 0$), $p_{1a}$ is the frequency of allele $a$ at locus $l$ in the reference sample, $n_i$ is the number of alleles defined in the sample at locus $l$ (the number of individuals times the ploidy level minus the number of missing alleles), and $\Sigma c_1$ stands for the sum over the homologous chromosomes.
of individual \(i\). Here, the term involving \((n_1 - 1)\) is a sampling bias correction. The program calculates the pair wise relationship between animals \(i\) and \(j\) (\(a_{ij}\)) leaving the diagonal elements blank (\(a_{ii}\)), thus self-coancestry had to be estimated as: \(F_k = 1 + 0.5a_{ij}\), where \(a_{ij}\) is relationship between parents \(i\) and \(j\) of individual \(k\).

The third method used MCMC (Markov Chain Monte Carlo simulations) to estimate genetic relationship between animals for a selected number of 39 SNP markers from chromosome 1, with minor allele frequency above 0.1 (selected SNP method - SNPC). This limitation was imposed due to time-extensive properties of the MCMC method. Software package Citius\[5,6\] was used to apply the MCMC method to calculate multilocus genotype probabilities and to analyse genes shared identical by descent (IBD). IBD matrices were calculated in 9 points along the analysed fragment of chromosome 1. Afterwards they were averaged into one G-matrix, that was used for further computations.

Estimation of variance components and breeding values

Variance components were estimated separately for each time point (0, 132, 265, 397, 530), with ASREML [7] using the following model:

\[
y_i = \mu + a_i + e_i
\]

Where: \(y_i\) - analysed trait, \(a_i\) - random additive genetic effect of animal \(i\); \(e_i\) - random residual effect.

The covariance structure was specified as:

\[
E\left[\begin{array}{c} a \\ e \end{array}\right] = \left[\begin{array}{c} 0 \\ 0 \end{array}\right] \quad \text{and} \quad V\left[\begin{array}{c} a \\ e \end{array}\right] = \left[\begin{array}{cc} \sigma_a^2 & 0 \\ 0 & \sigma_e^2 \end{array}\right]
\]

where: \(\sigma_a^2\) - additive genetic variance, \(\sigma_e^2\) - residual variance, \(G\) - genetic relationship matrix, \(I\) - identity matrix.

The analysis was performed with three types of genetic covariance matrices (\(G\)) based on: pedigree (PB method), and SNP markers (methods SNPL and SNPC). Quadratic regression of predicted breeding values on time, extracted from ASREML, in the first five time points was applied to estimate least square regression coefficients for each animal. Subsequently, the estimated regression coefficients were used to predict the unknown breeding values in the 6th time point (time 600) using the following formula:

\[
y_{600,i} = \hat{\beta}_0 + \hat{\beta}_1 x_i + \hat{\beta}_2 x_i^2
\]

where: \(y_{600,i}\) is the breeding value in time point 600; \(\hat{\beta}_0, \hat{\beta}_1, \hat{\beta}_2\) are least square regression coefficients, estimated for animal \(i\).

Results

Variance components

Regardless of the method used, genetic and residual variances increased with time (Table 1). Estimates of

| T0    | T132   | T265   | T397   | T530   |
|-------|--------|--------|--------|--------|
| Genetic variance | 0.05   | 0.33   | 1.81   | 7.49   | 19.23 |
| SNPL  | 0.05   | 0.35   | 2.10   | 8.84   | 23.32 |
| SNPC  | 0.04   | 0.28   | 1.62   | 6.50   | 16.21 |
| Residual variance | 0.05   | 0.35   | 2.05   | 8.62   | 21.32 |
| SNPL  | 0.04   | 0.27   | 1.53   | 6.35   | 14.98 |
| SNPC  | 0.06   | 0.41   | 2.30   | 9.58   | 23.76 |
| Heritability | 0.50   | 0.48   | 0.46   | 0.46   | 0.47  |
| SNPL  | 0.53   | 0.56   | 0.57   | 0.58   | 0.60  |
| SNPC  | 0.40   | 0.40   | 0.41   | 0.40   | 0.40  |

Table 2 Correlation between breeding values in five time points (T0, T132, T265, T397 and T530), estimated with a genetic covariance matrix based on 90 SNPs from chromosome 1 (SNPL method).

| T0    | T132   | T265   | T397   | T530   |
|-------|--------|--------|--------|--------|
| T0    | 0.987  |        |        |        |
| T132  | 0.939  | 0.981  |        |        |
| T265  | 0.862  | 0.929  | 0.982  |        |
| T397  | 0.818  | 0.894  | 0.961  | 0.995  |
| T530  | 0.824  | 0.899  | 0.964  | 0.995  |

Table 3 Correlation between breeding values in five time points (T0, T132, T265, T397 and T530) estimated with a genetic covariance matrix based on a selected number of SNPs from chromosome 1, with minor allele frequency >0.1 (SNPC method).

| T0    | T132   | T265   | T397   | T530   |
|-------|--------|--------|--------|--------|
| T0    | 0.987  |        |        |        |
| T132  | 0.940  | 0.981  |        |        |
| T265  | 0.865  | 0.932  | 0.983  |        |
| T397  | 0.824  | 0.899  | 0.964  | 0.995  |
| T530  | 0.792  | 0.879  | 0.956  | 0.994  |

Table 4 Correlation between breeding values in five time points (T0, T132, T265, T397 and T530) estimated with a genetic covariance matrix based on pedigree records (PB method).
genetic variance were lower for the SNPC method than the PB or SNPL method. In case of the PB method heritability decreased from 0.51 (time point 0) to 0.47 (time point 530). On the other hand the SNPL method resulted in genetic variance increasing more than the residual variance, which resulted in an increase of heritability from 0.53 (time point 0) to 0.60 (time point 530). Heritability estimates for the SNPC method did not differ much between the time points and were between 0.40 and 0.41. Correlations between breeding values in the different time points were high - between 0.82 and

|      | PB | SNPL | SNPC |
|------|----|------|------|
| Correlation | 0.65 | 0.75 | 0.80 |
| Regression  | 0.93 | 0.79 | 0.92 |
0.99 for the SNPL and SNPC methods (Table 2 and Table 3) and between 0.79 and 0.99 for the PB method (Table 4) reached around 0.98.

**Breeding values**

The variance of predicted breeding values in the time point 600 was the lowest for the PB method (17.44), the highest for the SNPL method (27.94), and moderate for the SNPC method (20.42). In contrast to the PB in case of the SNP based methods there was considerable variation in breeding values within FS families (Figure 1). Correlations between breeding values in time point 600, estimated with the three methods were between 0.82 and 0.86. When comparing the list of top 20 nonphenotyped animals selected with the three methods with the true list of top 20 nonphenotyped animals from the simulation (as provided by organizers), than the PB method had only 30% of individuals in common. Higher agreement was found for SNP based methods: 45% and 50% for the SNPC and the SNPL methods, respectively. Accuracy of breeding values (correlation between predicted and true breeding values) for the 1000 nonphenotyped individuals in the time point 600 was the lowest for the PB method (0.65), higher for the SNPL method (0.75) and the highest for the SNPC method (0.80). Regression coefficients of true breeding values on predicted breeding values were between 0.79 - 0.93 (Table 5).

**Discussion**

The genetic variance estimated with the PB method was the closest to the true (simulated) one while variance components obtained with SNPL method were slightly overestimated. Underestimation of genetic variance with the SNPC method can be due to ignoring a part of SNPs. Changes of heritability estimates in case of the SNPL method could be due to overestimation of genetic variance which was higher for higher phenotypic variance. Genomic breeding values usually show bias, which is a consequence of using marker instead of QTL effects [8]. This bias exist also in our results - regression of true breeding values on predicted breeding values is much below 1.

Rather high variation of breeding values could be partly due to Mendelian variation and partly as a result of method inadequacy. Both SNPL and SNPC methods explored differences among animals within full-sib families but it is hard to decide which one should be preferred as one yielded higher accuracy but the second more correctly chose the top 20 animals.

It is also worth mentioning that the method for prediction of breeding values applied in this paper (quadratic regression) does not take into account the fact that the analysed trait will eventually reach its asymptotic value.

The restriction of using only one chromosome was imposed partially due to the fact that SNPC method is very computationally demanding and the SNPL method had a software limitation for the number of markers. This might have a drawback of our analysis as it neglects large part of the available SNP information. Nevertheless this simplified analysis allowed to predict breeding values with fairly high accuracy of 0.75 - 0.80. However because after the analysis it turned out that the first chromosome contained QTLs with the largest effect [1] it may be concluded that the result would have been much worse in other, practical situations.

In our analysis we used a concept of genetic relationship matrix to obtain genomic breeding values, which is similar to the method described by Zhang et al. [9]. Van Raden showed that reliabilities of GEBVs based on this approach are almost as high as in the Bayes B method [10]. The SNPL and SNPC methods, both assumed equal effects of all markers from chromosome I.

**Conclusions**

Application of SNP markers enables to differentiate breeding values within full sib families. Based on the comparison of true (simulated by organizers) breeding values in the time point 600 with our predictions it can be concluded that SNP based methods provided relatively good estimates. Even though only SNPs from chromosome 1 were used it was still possible to achieve fairly high accuracies. Most likely it was due to the fact that chromosome 1 contained the most significant QTLs affecting the analysed trait.

**Acknowledgement**

The authors would like to express their gratitude to Maciej Szydlowski for discussion and support with the software package Citius. This article has been published as part of BMC Proceedings Volume 4 Supplement 1, 2009: Proceedings of 13th European workshop on QTL mapping and marker assisted selection. The full contents of the supplement are available online at http://www.biomedcentral.com/1753-6561/4?issue=S1.

**Authors’ contributions**

SM: performed the analysis and drafted the manuscript. AW: performed the analysis and drafted the manuscript. TM: performed the analysis and drafted the manuscript. All authors read and approved the final manuscript.

**Competing interests**

The authors declare that they have no competing interests.

**Published:** 31 March 2010

**References**

1. Coster A, Bastiaansen J, Calus M, Maliepaard C, Bink M. QTLMAS 2009, Simulated dataset. Submitted to BMC 2009.
2. Hardy OJ, Vekemans X. SPAGeDi: a versatile computer program to analyse spatial genetic structure at the individual or population levels. Molecular Ecology Notes 2002; 2618-620.
3. Seaton G, Hernandez J, Grunchec J A, White I, Allen J, De Koning D J, Wei W, Berry D, Haley C, Knott S. GRIDQTL: a grid portal for QTL mapping of compute intensive datasets. Proceedings of the 8th World Congress on Genetics Applied to Livestock Production, Belo Horizonte, MG, Brasil 2006.
4. Loiselle BA, Sork VL, Nason J, Graham C: Spatial genetic structure of a tropical understory shrub, Psychotria officinalis (Rubiaceae). *American Journal of Botany* 1995, 82:1420-1425.

5. Szydlowski M: Citius: A program to apply Markov chain Monte Carlo method for multilocus analysis of large complex pedigrees - User Guide [http://jay.au.poznan.pl/~mczyd/citius/citius.pdf]. 2008.

6. Szydlowski M, Gengler N: Sampling genotype configurations in a large complex pedigree. *Journal of Animal Breeding and Genetics* 2008, 125:330-338.

7. Gilmour AR, Gogel BJ, Cullis BR, Thompson R: ASReml User Guide Release 2.0. VSN International Ltd, Hemel Hempstead, HP1 1ES, UK 2006.

8. Solberg TR, Sonesson AK, Woolliams JA, Meuwissen TH: Genomic selection using different marker types and densities. *Journal of Animal Science* 2008, 86:2447-2454.

9. Zhang Z, Todhunter RJ, Buckler ES, Van Vleck LD: Technical note: Use of marker-based relationships with multiple-trait derivative-free restricted maximal likelihood. *Journal of Animal Science* 2007, 85:881-885.

10. Van Raden PM: Efficient Methods to Compute Genomic Predictions. *Journal of Dairy Science* 2008, 91:4414-4423.

doi:10.1046/j.1471-8286.2002.00305.x

Cite this article as: Mucha et al.: Comparison of methods for estimation of genetic covariance matrix from SNP or pedigree data utilised to predict breeding value. *BMC Proceedings* 2010, 4(Suppl 1):S7.