Super No-Scale $\mathcal{F}$-$SU(5)$: A Dynamic Determination of $M_{1/2}$ and $\tan \beta$

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Abstract

We study the Higgs potential in No-Scale $\mathcal{F}$-$SU(5)$, a model built on the tripodal foundations of the $\mathcal{F}$-lipped $SU(5) \times U(1)_X$ Grand Unified Theory, extra $\mathcal{F}$-theory derived TeV scale vector-like particle multiplets, and the high scale boundary conditions of no-scale supergravity. $V_{\text{min}}$, the minimum of the potential following radiative electroweak symmetry breaking, is a function at fixed $Z$-Boson mass of the universal gaugino boundary mass $M_{1/2}$ and $\tan \beta$, the ratio of Higgs vacuum expectation values. The so-scale nullification of the bilinear Higgs soft term $B_\mu$ at the boundary reduces $V_{\text{min}}(M_{1/2})$ to a one dimensional dependency, which may be secondarily minimized. This “Super No-Scale” condition dynamically fixes $\tan \beta$ and $M_{1/2}$ at the local minimum minimorum of $V_{\text{min}}$. Fantastically, the walls of this theoretically established secondary potential coalesce in descent to a striking concurrency with the previously phenomenologically favored “Golden Point” and “Golden Strip”.

Keywords: No-Scale Supergravity, F-Theory, Vector-like Multiplets, Flipped SU(5), Grand Unification, Higgs Potential, Gauge Hierarchy

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1. Introduction and Background

We have recently demonstrated [1, 2] the unique phenomenological consistency and profound predictive capacity of a model dubbed No-Scale $\mathcal{F}$-$SU(5)$, constructed from the merger of the $\mathcal{F}$-lipped $SU(5)$ Grand Unified Theory (GUT) [3-5], two pairs of hypothetical TeV scale vector-like supersymmetric multiplets with origins in $\mathcal{F}$-theory [6-10], and the dynamically established boundary conditions of no-scale supergravity [11-15]. It appears that the no-scale scenario, particularly vanishing of the Higgs bilinear soft term $B_\mu$, comes into its own only when applied at an elevated scale, approaching the Planck mass [16]. $M_F$, the point of the second stage $SU(5) \times U(1)_X$ unification, emerges in turn as a suitable candidate scale only when substantially decoupled from the primary GUT scale unification of $SU(3)_C \times SU(2)_L$ via the modification to the renormalization group equations (RGEs) from the extra $\mathcal{F}$-theory vector multiplets [1, 2].

Taking a definition of $M_V = 1$ TeV for the new vector-like fields as an elemental model feature, we showed [1] that the viable parameter space consistent with radiative electroweak symmetry breaking (EWSB), limits on the flavor changing neutral current ($b \rightarrow s\gamma$) process and on contributions to the muon anomalous magnetic moment ($g - 2)_\mu$, runs...
sufficiently perpendicular to both the $B_\mu(M_F) = 0$ and centrally observed WMAP 7 cold dark matter (CDM) relic density contours that the non-trivial mutual intersection is a narrowly confined “Golden Point” with a universal gaugino boundary mass $M_{1/2}$ around 455 GeV, and a ratio $\tan\beta = 15$ of Higgs vacuum expectation values (vevs). Insomuch as the collision of top-down model based constraints with bottom-up experimental data effectively absorbs the final dynamic degree of freedom, this was labeled a No-Parameter Model.

Advancing from the “Golden Point” to the “Golden Strip” [2], we relaxed the definition of the vector-like mass and studied the impact of fluctuating key electroweak reference data ($\alpha_s, M_Z$) and the top quark mass $m_t$ about the error margins.

The most severe variation occurred for $m_t$, via its connection to the large Yukawa coupling essential by effectively treating $m_t$ as an additional input, selecting the appropriate value to restore a vanishing $B_\mu(M_F)$ at each point in the ($M_{1/2}, \tan\beta, M_V$) volume. The $(g-2)_\mu$ and $(b \to s\tau)$ constraints, both at their lower limits, were found to exert opposing pressures on $M_{1/2}$ due to operation of the former in alignment with, and the latter in counterbalance of, the Standard Model (SM) leading term. Cross cutting by the WMAP CDM measurement completed demarcation of the strip, running diagonally from about $(M_{1/2}, M_V) = (455,1020)$ GeV, to (481,691) GeV, with $\tan\beta = 15$ independently enforced for the full space. With parameterization freedom exhausted, the model was finally required to make a correlated postdiction for the top quark mass. The result, $m_t = 173.0 \pm 174.4$ GeV, is in fine accord with the measured value $173.1 \pm 1.3$ GeV [17]. The predicted range of $M_V$ is testable at the LHC, and the partial lifetime for proton decay in the leading $(e|\mu)^+\pi^0$ channels is $4.6 \times 10^{34}$ years, testable at the future Hyper-Kamiokande [18] and DUSEL [19] experiments.

2. The Super No-Scale Mechanism

In the present work we volunteer a small step backward to amplify a giant leap forward. Having established practical bounds on the vector-like mass, we revert to a single conceptual universe, ostensibly our own or one of sufficient phenomenological proximity, with $M_V = 1000$ GeV, and $m_t = 173.1$ GeV. Minimization of the Higgs potential with respect to the neutral up-like and down-like Higgs components $H_u$ and $H_d$ imposes a pair of constraint equations which may be used to eliminate any two free parameters of the set $M_{1/2}, B_\mu, \tan\beta \equiv (H_u)/(H_d)$, and the supersymmetry (SUSY) preserving bilinear Higgs mass term $\mu$. The overall magnitude of the Higgs vev $v \equiv \sqrt{(H_u)^2 + (H_d)^2}$ $\approx 174$ GeV is considered to be experimentally constrained by measurement of the gauge couplings and Z-Boson mass. Typically, one will solve for $\mu(M_Z)$ and $B_\mu(M_Z)$ in terms of the constrained Higgs vevs and $\tan\beta$, at fixed $M_{1/2}$. We consider though that the no-scale boundary condition $B_\mu(M_F) = 0$ fixes the value of $B_\mu$ at all other scales as well via action of the renormalization group. Restricting then to just the solution subset for which $B_\mu(M_Z)$ given by EWSB stitches cleanly onto that run down under the RGEs from $B_\mu(M_F) = 0$, $\tan\beta$ (or alternatively $\mu$) becomes an implicit function of the single modulus $M_{1/2}$.

Concretely, we shall consider that the first EWSB constraint absolutely establishes $\mu$, and that the second gives a line of parameterized solutions for the functional relationship between $M_{1/2}$ and $\tan\beta$. We therefore distinguish the residual freedom in the dynamic modulus $M_{1/2}$ and parameter $\tan\beta$ by the ability to exert direct influence on the Higgs potential within a single physical parameterization.

The crucial observation is that the minimization of the Higgs potential is therefore at this stage incomplete. In no-scale supergravity, the specific structure of the Kähler potential $K$ leads to a contribution to the scalar potential which is is zero and flat at tree level, so that the gravitino mass $M_3/2$, or by proportional equivalence $M_{1/2}$, is to be determined dynamically by radiative corrections. In order to finish specification of the physical vacuum, we must then secondarily minimize the Higgs potential with respect to the dependency on $M_{1/2}$, a dependency which is embodied in the bulk proportionality of the full low energy mass spectrum to this SUSY breaking parameter [12,13]. At this locally smallest value of $V_{\text{min}}(M_{1/2})$, which we dub the minimum minimorum, the dynamic determination $M_{1/2}$ is established. Moreover, the implicit dependence of the parameter $\tan\beta$ on $M_{1/2}$ means that its value is also simultaneously provided by the system dynamics. Henceforth, the imposition of $dV_{\text{min}}/dM_{1/2} = 0$ on the Higgs potential will be referred to as the “Super No-Scale” condition.

We emphasize that the justification for this procedure traces back to the fact that the soft SUSY breaking mass $M_{1/2}$ is related to the F-term of a
3. F-SU(5) Models

In the Flipped SU(5) GUTs, the gauge group is SU(5) × U(1)X, which embeds in SO(10). Gauge coupling unification near 10^{16} GeV strongly suggests the existence of a Grand Unified Theory (GUT). In minimal SUSY SU(5) models there are problems with doublet-triplet splitting and dimension five proton decay by colored Higgsino exchange. These difficulties are elegantly overcome in Flipped SU(5) GUT models via the missing partner mechanism. The generator U(1)Y is defined for fundamental five-plets as −1/3 for the triplet members, and +1/2 for the doublet. The hypercharge is given by Q_{Y} = (Q_{X} - Q_{Y'})/5. There are three families of Standard Model (SM) fermions, a pair of ten-plet Higgs for breaking the GUT symmetry, and a pair of five-plet Higgs for EWSB.

Historically, the first flipped F-theory SU(5) GUT was constructed in Ref. [21], and further aspects of flipped SU(5) F-theory GUTs have been considered in [21, 22]. We introduce in addition, vector-like particle multiplets, derived likewise in the context of F-theory model building, to address the “little hierarchy” problem, altering the beta coefficients of the renormalization group to dynamically elevate the secondary SU(5) × U(1)X unification at M_{F} to near the Planck scale, while leaving the SU(3)C × SU(2)L unification at M_{Z} close to the traditional GUT scale. In other words, one obtains true string-scale gauge coupling unification in free fermionic string models [23] or the decoupling scenario in F-theory models [24, 25]. To avoid a Landau pole for the strong coupling constant, we are restricted around the TeV scale to one of the following two multiplet sets:

\[
\begin{align*}
(XX_{F(10,1)} &\equiv (X_{Q}, XD^{c}, XN^{c}), \quad X_{F(10,1)}^{c} ) \\
(X_{l(1,5)}, X_{l(1,5)}^{c} &\equiv XE^{c})
\end{align*}
\]

Prior, XQ, XD^{c}, XE^{c}, XN^{c} have the same quantum numbers as the quark doublet, right-handed down-type quark, charged lepton, and neutrino, respectively. We have argued [2] that the eminently feasible near-term detectability of these hypothetical fields in collider experiments, coupled with the distinctive flipped charge assignments of the multiplet structure, represents a smoking gun signature for Flipped SU(5), and have thus coined the term flippons to collectively describe them. Immediately, our curiosity is piqued by the announcement of the DO collaboration that vector-like quarks have been excluded up to a bound of 693 GeV, corresponding to the lower edge of our golden strip. We here consider only the Z2 set, although discussion for the Z1 set, if supplemented by heavy threshold corrections, will be similar.

4. No-Scale Supergravity

The Higgs boson, being a lorentz scalar, is not stable in the SM against quadratic quantum mass corrections which drive it toward the dominant Planck scale, some seventeen orders of magnitude above the value required for consistent EWSB. Supersymmetry naturally solves this fine tuning problem by pairing theiggs with a chiral spin-1/2 “Higgsino” partner field, and following suit with a corresponding bosonic (fermionic) superpartner for all fermionic (bosonic) SM fields, introducing the full set of quantum counter terms. Localizing the
supersymmetry algebra, which includes the generator of spacetime translations (the momentum operator), induces general coordinate invariance, producing the supergravity (SUGRA) theories.

Since we do not observe mass degenerate superpartners for the known SM fields, SUSY must itself be broken around the TeV scale. In the traditional framework, supersymmetry is broken in the hidden sector, and the effect is mediated to the observable sector via gravity or gauge interactions. In GUTs with minimal gravity mediated supersymmetry breaking, called mSUGRA, one can fully characterize the supersymmetry breaking soft terms by four universal parameters (gaugino mass $M_{1/2}$, scalar mass $M_0$, trilinear coupling $A$, and the low energy ratio $\tan\beta$), plus the sign of the Higgs bilinear mass term $\mu$.

No-Scale Supergravity was proposed [11–15] to address the cosmological flatness problem. It may be verified for the simple example Kähler potential

$$K = -3 \ln(T + \mathcal{T} - \sum_i \Phi_i^* \Phi_i),$$

where $T$ is a modulus field and $\Phi_i$ are matter fields, that the no-scale boundary conditions $M_0 = A = B_\mu = 0$ are enforced automatically, while $M_{1/2} > 0$ is allowed, as is indeed required for SUSY breaking. All low energy scales are dynamically generated by quantum corrections, i.e. running under the RGEs, to the classically flat potential. Additionally, the tree level vacuum energy vanishes automatically. The fiercely reductionist no-scale picture moreover inherits an associative weight of motivation from its robustly generic and natural appearance in string based constructions.

The simple form of Eq. (2) has been independently derived in both weakly coupled heterotic $E_8 \times E_8$ string theory [28] and for strong coupling, in the leading order compactification of M-theory on $S^4/Z_2$ [24]. In both cases, the Yang-Mills fields span a ten dimensional space-time. However, this potential is not obtained directly out of F-theory, as represented for example by the strong coupling lift from Type IIB intersecting D-brane model building with D7- and D3-branes [20, 28, 30], where the Yang-Mills fields on the D7-branes occupy an eight dimensional space-time. Nevertheless, it is certainly possible in principle to calculate a gauge kinetic function, Kähler potential and superpotential in the context of Type IIB intersecting D-brane model building, and the F-theory could thus admit a more general definition of no-scale supergravity, as realized by a Kähler potential like

$$K = -\ln(S + \mathcal{S}) - \ln(T_1 + \mathcal{T}_1) - \ln(T_2 + \mathcal{T}_2) - \ln(T_3 + \mathcal{T}_3),$$

where only three of the moduli fields $S$ and $T_i$ may yield non-zero F-terms.

However, the $\mathcal{F}$-$SU(5)$ type models under discussion have been constructed locally in F-theory [1, 8], and without a corresponding consistent global construction, we do not know the concrete Kähler potential of the SM fermions and Higgs fields, and cannot by this means explicitly calculate the supersymmetry breaking scalar masses and trilinear soft terms. Essentially then, we aim to study an F-theory inspired variety of low energy SUSY phenomenology, remaining agnostic as to the details of the Kähler structure. By studying the simplest no-scale supergravity, we may still however expect to encapsulate the correct leading order behavior. Should the favorable qualitative phenomenology of this lowest order analysis prove persistent, our future attention will be directed toward quantitatively specific no-scale supergravity generalizations.

5. The Higgs Minimum Minimorum

We now proceed to specifically implement, within the context of the $\mathcal{F}$-$SU(5)$ construction, the Super No-Scale mechanism described in Section (2). Again, for a given Higgs vev, i.e. for a fixed Z-Boson mass, we establish $\tan\beta$, by application of the two EWSB consistency conditions, to be an implicit function of the universal gaugino boundary mass $M_{1/2}$, along a continuous string of minima of the broken Higgs potential $V_{\text{min}}$, which are likewise labeled by their value of $M_{1/2}$. It is with respect to this line of solutions that we seek to establish a local secondary minimum minimorum of the Higgs potential $V_{\text{min}}(M_{1/2})$.

We employ an effective Higgs potential in the ’t Hooft-Landau gauge and the $\overline{\text{DR}}$ scheme, given summing the following neutral tree ($V_0$) and one loop ($V_1$) terms.

$$V_0 = (\mu^2 + m_{H_u}^2)(H_u^0)^2 + (\mu^2 + m_{H_d}^2)(H_d^0)^2 - 2\mu B_\mu H_u^0 H_d^0 + \frac{g_2^2 + g_Y^2}{8} [(H_u^0)^2 - (H_d^0)^2]^2$$

$$V_1 = \sum_i \frac{n_i}{64\pi^2} m_i^2(\phi) \left( \frac{m_i^2(\phi)}{Q^2} - \frac{3}{2} \right).$$

Prior, $m_{H_u}^2$ and $m_{H_d}^2$ are the soft SUSY breaking masses of the Higgs fields $H_u$ and $H_d$, $g_2$ and $g_Y$ are
the gauge couplings of $SU(2)_L$ and $U(1)_Y$, $u_i$ and $m_i^2(\phi)$ are the degree of freedom and mass for $\phi_i$, and $Q$ is the renormalization scale. In particular, the soft breaking parameters $m_H^2$, $m_{H_d}^2$, and $m_{H_u}^2$ are not free parameters, but rather functions of the universal gaugino boundary mass $M_{1/2}$, run down to the point of electroweak symmetry breaking under the renormalization group. We include the complete Minimal Supersymmetric Standard Model (MSSM) contributions to one loop, following Ref. [31], although the result is phenomenologically identical accounting only the leading top and partner stop terms. Since the minimum of the electroweak (EW) Higgs potential $V_{\text{min}}$ depends implicitly on $M_{1/2}$, the gravitino mass is determined by the Super No-Scale condition $dV_{\text{min}}/dM_{3/2} = 0$. Being, however, that $M_{1/2}$ is proportional to $M_{3/2}$, it is equivalent to employ $M_{1/2}$ directly as our modulus parameter, as previously described. All other SUSY breaking soft terms will subsequently be derived from this single dynamically determined value.

Factors explicit within the potential are obtained from our customized extension of the SuSpect 2.34 [32] codebase, including a self-consistency assessment [1] on $B_\mu = 0$. We apply two-loop RGE running for the SM gauge couplings, and one-loop running for the SM fermion Yukawa couplings, $\mu$ term and soft terms.

Studying $V_{\text{min}}$ generically in the $(M_{1/2}, \tan \beta)$ plane, no point of secondary minimization is readily apparent in the strong, roughly linear, downward trend with respect to $M_{1/2}$ over the region of interest. However, the majority of the plane is not in physical communication with our model, disrespecting the fundamental $B_\mu = 0$ condition. Isolating only the compliant $B_\mu = 0$ contour within this surface, a parabola is traced, the nadir of which is in excellent agreement with our original golden point, as shown in Fig. (1A). Restoring parameterization freedom to $(M_Y, m_0)$, we may scan across the corresponding golden point of each nearby universe variant, reconstructing in their union the previously advertised golden strip, as in Fig. (1B). Notably, the theoretical restriction on $\tan \beta$ remains stable against variation in these parameters, exactly as its experimental counterpart.

We find it quite extraordinary that the phenomenologically preferred region rests precisely at the curve’s locus of symmetric inflection. Note in particular that it is the selection of the parabolic $B_\mu = 0$ contour out of the otherwise uninteresting $V_{\text{min}}(M_{1/2}, \tan \beta)$ inclined surface which allows a clear minimum minimorum to be established. We reiterate that consistency of the dynamically positioned $M_{1/2}$ and $\tan \beta$ with the golden strip implies broad consistency with all current experimental data, within the resolution of the methodology and numerical tools employed.
A strongly linear relationship is observed between the SUSY and EWSB scales with $M_{\text{EWSB}} \simeq 1.44 M_{1/2}$, such that a corresponding parabolic curve may be visualized. There is a charged stau LSP for $\tan \beta$ from 16 to 22, and we connect points with correct EWSB smoothly on the plot in this region. If $\tan \beta$ is larger than 22, the stau is moreover tachyonic, so properly we must restrict all analysis to $\tan \beta \leq 22$.

6. Additional Phenomenology

No-Scale $\mathcal{F}$-SU(5) features, quite stably, the distinctive mass hierarchy $m_\chi < m_\tilde{q} < m_\tilde{g}$ of a light stop and gluino, both comfortably lighter than all other squarks. Typical ballpark mass values consistent with the dynamic determination of $M_{1/2} \sim 450 \text{ GeV}$ are $m_\tilde{t} \sim 500 \text{ GeV}$, $m_\tilde{q} \sim 625 \text{ GeV}$, and $m_\tilde{g} \sim 1000 \text{ GeV}$. The lightest neutralino, which is $\sim 99.8\%$ Bino, may feature a mass somewhat less than 100 GeV. For direct comparison, we reprint the detailed spectrum of the original “Golden Point” of Ref. 1 in Table (1).

We suggest that the spectrum so described thus far survives the advancing detection limits being posted by early LHC results, which we further point out are typically tuned to the mSUGRA/CMSSM context, often also with particular assumptions applied to $\tan \beta$. However, the margin of escape may be narrow, even for the meager 35 pb$^{-1}$ of integrated luminosity heretofore described. Specifically, Figure (2) of Ref. [33] seems to imply a 95% lower exclusion boundary of slightly more than 1 TeV for gluino masses in our favored range. The approach taken by this example analysis does at least take a step toward probing No-Scale $\mathcal{F}$-SU(5) by the claim of model independence from the mSUGRA/CMSSM orthodoxy, but there are several peculiar assumptions made with regards to the spectrum that suggest the prudence of a certain circumspection in interpretation of any quoted bottom line results. In particular, the lightest neutralino is made massless, and all SUSY fields besides the gluino and the first two squark generations, i.e. all sleptons, all Higgs, all other neutralino components and the third generation of squarks, are decoupled by assignment of an ultra-heavy 5 TeV mass. A closer inspection of the data files published by the ATLAS collaboration along with the cited report confirms that all decay modes are eliminated besides those to the massless neutralino plus hadronic jets or leptons.

We maintain some ever present anticipation that the discovery of supersymmetry at the LHC could be imminent, a sentiment which an optimistic reading of the early reports from ATLAS and CDF might be taken to reinforce. We should remark, however, that relaxation of the fixed $M_F$ and $m_1$ mass values adopted here for simplicity and concreteness will allow the migration, if necessary, to a somewhat heavier spectrum. This may be accomplished without wholesale rejection of the underlying model (No-Scale $\mathcal{F}$-SU(5)) or method of analysis (the Super No-Scale mechanism) which have been our focus in the present work. We defer for future work a comprehensive mapping of such alternative configurations, which in their union compose the complete viable model space.

7. The Gauge Hierarchy Problem

The “gauge hierarchy problem” represents, in actuality, the clustering of multiple related difficulties into a single amalgamation, rather than a single isolated problem with a correspondingly isolated solution. Not only must we explain stabilization of the EW scale against quantum corrections, but we must also explain why this scale and TeV-sized SUSY breaking soft-terms are “initially” positioned so far below the Planck mass. These latter components of the gauge hierarchy problem are the more subtle. In their theoretical pursuit, we do not though feign ignorance of established experimental boundaries, taking the phenomenologist’s perspective that pieces fit already to the puzzle stipulate a partial contour of those yet to be placed. Indeed, careful knowledge of precision EW scale physics, including the strong and electromagnetic couplings, the Weinberg angle and $M_Z$ are required even to run the one loop RGEs. In the second loop, one requires also minimally the leading top quark Yukawa coupling, as deduced from $m_t$, and the overall magnitude of the Higgs vev $v$, established in turn from measurement of the effective Fermi coupling, or from $M_Z$ and the electroweak couplings.

Reading the RGEs up from $M_Z$, we take unification of the gauge couplings as evidence of a GUT. Reading them in reverse from a point of high energy unification, we take the heaviness of the top quark, via its large Yukawa coupling, to dynamically drive the term $M_H^2 + \mu^2$ negative, triggering spontaneous collapse of the tachyonic vacuum, i.e. radiative electroweak symmetry breaking. As we have elaborated in Section (2), the minimization
of this potential with respect to the neutral components of $H_u$ and $H_d$ at fixed Z-Boson mass allows one to absolutely establish a numerical value for $\mu$, in addition to a line of of continuously parameterized solutions for the functional relationship between $M_{1/2}$ and $\tan \beta$.

Strictly speaking though, we must recognize that having effectively exchanged input of the Z-mass for a constraint on $\mu(M_Z)$, we dynamically establish the SUSY breaking soft term $M_{1/2}$ and $\tan \beta$ within the electroweak symmetry breaking vacua, i.e. with fixed $v \simeq 174$ GeV. By employing only values of $\mu$ consistent with the physically constrained Higgs vev, the current construction does not then intrinsically address the $\mu$ problem, i.e. the reason for the proximity of the SUSY preserving Higgs mass parameter $\mu$ to the electroweak scale and the soft SUSY breaking mass term $M_{1/2}$. This problem is however ubiquitous to all supersymmetric model constructions, and there is no reason to prevent a parallel embedding of the usual proposals for addressing the $\mu$ problem alongside the Super No-Scale mechanism. Likely candidates for the required suppression relative to the Planck scale would include the invocation of powers of F-term vevs $(\langle F \rangle/M_{Pl})$ via the Giudice-Masiero mechanism [34], or the introduction of a SM singlet Higgs field as in the next-to-minimal supersymmetric standard model (NMSSM), or as a final example, the consideration of an anomalous $U(1)_A$ gauge symmetry to be realized out of a string theoretic model building approach [35].

Acknowledging that we have not here fundamentally explained the TeV-scale correlation of $\mu$ and $\mu$ to the modulus $M_{1/2}$, we are nevertheless content to justify the values employed by the success of the globally consistent picture which they facilitate. In any event, a clear conceptual distinction should be maintained between the simple parameters $\mu$ and $M_0$ and the string theoretic modulus $M_{1/2}$, the latter being uniquely eligible for dynamic stabilization under application of the Super No-Scale mechanism. The current proposal may reach somewhat farther though, than even it first appears. Having predicted $M_T$ as an output scale near the reduced Planck mass, we are licensed to invert the solution, taking $M_T$ as a high scale input and dynamically address the gauge hierarchy through the standard story of radiative electroweak symmetry breaking. This proximity to the elemental high scale of (consistently decoupled) gravitational physics, arises because of the dual flipped unification and the perturbing effect of the TeV multiplets, and is not motivated in standard GUTs.

Operating the machinery of the RGEs in reverse, we may transmute the low scale $M_Z$ for the high scale $M_T$, emphasizing that the fundamental dynamic correlation is that of the ratio $M_Z/M_T$, taking either as our input yardstick according to taste. For fixed $M_T \simeq 7 \times 10^{17}$ GeV, in a single breath we receive the order of the electroweak scale, the $Z$-mass, the Higgs bilinear coupling $\mu$ and the Higgs vevs, all while dynamically tethering this derived scale to the soft SUSY breaking parameter $M_{1/2}$ via the action of the secondary minimization $dV_{\text{min}}/dM_{1/2} = 0$. All other dependent dimensional quantities, including the full superparticle mass spectrum likewise then fall into line. It is in this sense that the Super No-Scale mechanism, as applied to the present No-Scale $F$-$SU(5)$ construction, may contribute to an understanding of the issues composing the gauge hierarchy problem.

8. Conclusion

In this Letter, we have explored the Super No-Scale condition, that being the dynamic localization of the minimum minimorum of the Higgs potential, i.e. a locally smallest value of $V_{\text{min}}(M_{1/2})$, such that both $\tan \beta$ and $M_{1/2}$ are determined. The stabilized supersymmetry breaking and electroweak scales may both be considered as dependent output of this construction, thus substantively addressing the gauge hierarchy problem in the No-Scale
The collection of TeV scale boundaries for the soft terms in SUSY physics as a simple shell game by manual selection, and moreover achieving TeV scale EW and N-internal SU(5) to stabilize if viewed as a low energy supergravity theory seems a hoax, requiring horrendous fine tuning for a "golden point" and "golden strip". By comparison, the standard MSSM construction seems a hoax, requiring horrendous fine tuning to stabilize if viewed as a low energy supergravity theory, and moreover achieving TeV scale EW and SUSY physics as a simple shell game by manual selection of TeV scale boundaries for the soft terms $M_{1/2}$, $M_0$, and $A$. It is remarkable that despite featuring more freely tunable parameters, these constructions are finding it increasingly difficult to reconcile their phenomenology with early LHC data.

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