Modeling Time-Resolved Kinetics in Solids Induced by Extreme Electronic Excitation

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The authors present a concurrent Monte Carlo (MC)–molecular dynamics (MD) approach to modeling matter response to excitation of its electronic system at nanometric scales. The two methods are combined on-the-fly at each time step in one code, TREKIS-4. The MC model describes the arrival of irradiation (a photon, an electron, or a fast ion). It traces induced cascades of secondary electrons and holes, and their energy exchange with atoms due to scattering. The excited atomic system is simulated with an MD model. An efficient way is proposed to account for nonthermal effects in the electron-atom energy transfer in covalent materials via the conversion of the potential energy of the electron ensemble into the kinetic energy of atoms. Such a combined MC–MD approach enables a time-resolved tracing of the excitation kinetics of both, the electronic and atomic systems, and their simultaneous response to a deposited dose. As a proof-of-principle, it is shown that the proposed method describes atomic dynamics after X-ray irradiation in good agreement with tight-binding MD. The model also allows gaining insights into the atomic system behavior during the energy deposition from a nonequilibrium electronic system excited by an ion impact.

1. Introduction

Various types of irradiation causing initial extreme electronic excitation are employed for research and practical applications: photon, electron, and ion beams. Creating a highly excited state of matter,[1,2] femtosecond X-ray free-electron laser (FEL) pulse irradiation is used to process materials for nanotechnology, biophysics research, and production and studies of exotic states of matter such as warm dense matter.[1–5] Providing molecular imaging with unprecedented time-resolution on the order of a few femtoseconds, two-color FEL beams are applied to investigate the temporal kinetics of fundamental processes in matter and molecules under extreme electronic excitations.[1–5]

Irradiation with electrons is used in studies of material properties. It has a practical interest for electron microscopy, where electrons irradiating the target being imaged lead to degradation of the material.[6] Ultrafast electron diffraction recently found many practical applications, allowing to achieve femtosecond resolution to study fundamental effects in matter.[7,8]

Swift heavy ions (SHI) impacts modify materials within nanometric proximity of their trajectory, which makes them a unique tool for nanotechnological applications.[9,10] Irradiation with heavy ions is applied for creation of nanopores and membranes, used, e.g., for medical diagnostics.[11] SHIs are used in biology and medicine for tumor treatments[12,13] and for modeling cosmic rays’ effects.[14]

Transient processes in highly excited targets push standard models beyond their limits and motivate the development of new approaches,[15] forming fundamental interest in basic research. All these applications, resulting from the rapid and extreme excitation of the electronic system, require detailed modeling for a deeper understanding and control of the occurring processes.

Excitation of an electronic system by any of the abovementioned sources triggers a sequence of processes, starting with an elastic and inelastic scattering of fast electrons. The elastic scattering provides energy exchange with target atoms without secondary electron excitation. The inelastic one generates new electrons and holes in the core shells or the valence/conduction band of the material.[15,16] Typically, such processes occur at femtosecond timescales, cooling electrons within sub-picoseconds.

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Upon relaxation of the electronic system, the target atoms react to the energy transferred at picosecond to nanosecond timescales.\textsuperscript{[17,18]} Finally, after cooling of the atomic system, the target may be left in a structurally modified state, observable experimentally.\textsuperscript{[1,9]}

In the last decade, it became apparent that the standard calculations of the total deposited dose are not sufficiently precise to describe the local material modifications. This methodological limitation required the description of microscopic effects. Nanotechnological applications such as DNA modifications\textsuperscript{[24,25]} require a more detailed understanding of the microscopic processes involved. The quest for ever-increasing precision inevitably leads to the quest for a deeper understanding of the fundamental processes of damage formation caused by the excited electronic excitation, and the development of appropriate models.\textsuperscript{[18]}

This stimulated the development of hybrid and multiscale models that are becoming more and more common in applications. Such models combine a few different approaches into one code, tracing various aspects of the problem.\textsuperscript{[18]} Each model covers its own characteristic scales, for example, ultrashort time scales may be described with precise ab initio approaches, whereas macroscopic timescales may be traced with more approximate continuous (thermodynamic) models.\textsuperscript{[18]} In a more general case, in a hybrid approach, each model describes its own processes under appropriate conditions. For example, different subsystems (electrons and ions) may be described with different methods.

In the next section, we will describe TREKIS-4, the hybrid approach developed here, placing it in the context of modern existing hybrid and multiscale codes. We present a novel approach to the coupling of electrons and atoms in simulations. The simple, efficient, and precise scheme proposed enables advances in the modeling of materials response to various types of radiation causing a strong primary disturbance of the electronic system.

We demonstrate examples of the application of this approach to the description of an early stage of material response to an X-ray pulse and swift heavy ion irradiation. The combined approach allows us to gain an insight into the stage of overlapping electronic and atomic kinetics, which was not possible to obtain with previous state-of-the-art approaches, proving the versatility and capability of the proposed methodology.

2. Model

TREKIS-4 (which stands for time-resolved kinetics in irradiated solids) is a hybrid model combining two different methodologies (on-the-fly): Monte Carlo (MC) model with molecular dynamics (MD) simulations. The Monte Carlo module traces i) the incident particle penetration (which may be a photon, an electron, a positron, or an ion, in the current implementation); ii) transport of all secondary excited electrons; iii) kinetics of electronic holes; and iv) transport of emitted photons. The MD module of TREKIS-4 simulates the dynamics of target atoms triggered by the energy deposition from the electrons and holes. Such a combination allows tracing all essential processes, responsible for damage formation in a target under irradiation, e.g., phase transitions under femtosecond X-ray pulse irradiation, or formation of nanometric tracks after penetration of a swift heavy ion, as will be discussed in Section 3.

Earlier attempts combined MC and MD models sequentially: output data from MC simulations of electronic kinetics were passed as initial conditions to MD modeling of atomic response.\textsuperscript{[26–28]} For example, TREKIS-3 and earlier versions of the code were purely Monte Carlo codes, applicable to nonrelativistic swift heavy ions only. Calculated energy distributions were then manually passed into a separate MD code as initial conditions.

By contrast, TREKIS-4 executes both models in parallel. As will be described below, the data are exchanged at each time step of the simulation. The idea is similar to the two-temperature model (TTM) combination with MD, where the state of the electronic system is simulated with a temperature diffusion equation, while the atomic system is traced with MD.\textsuperscript{[29,30]} TTM–MD is currently a standard tool for simulation of laser-irradiated damage in metals, but it proved insufficient for modeling SHI impacts and resulted in the need to use adjustable parameters: most often, the electron–phonon coupling coefficient is fitted to reproduce experimental data on the track radius.\textsuperscript{[31]} It is also more complicated to apply TTM–MD to nonmetallic targets.\textsuperscript{[30,32,33]} In contrast to TTM, Monte Carlo modeling is fully capable of tracing nonequilibrium and ballistic electronic transport, effects of valence holes in nonmetallic materials, core holes kinetics, transport of photons, and it does not require fitting parameters.\textsuperscript{[34]}

A similar idea for a concurrent MC–MD scheme was previously used in a few codes, such as, e.g., MBN Explorer,\textsuperscript{[35]} XTANT,\textsuperscript{[36,37]} and XMDYN.\textsuperscript{[38]} MBN Explorer uses MD simulation of atomic motion in biological samples and kinetic MC simulations of various chemical processes. It does not explicitly trace secondary electron and holes transport, approximating electronic processes with rate equations instead. XMDYN code combines molecular dynamics simulations of both, ions and electrons, in plasma created by irradiation of samples with femtosecond X-ray pulses, with Monte Carlo simulation tracing atomic processes such as Auger and radiative cascades. It assumes a plasma limit, tracing only highly energetic particles, and not processes in solid targets such as phase transitions. XTANT code combines tight-binding MD with MC tracing of X-ray photons and nonequilibrium electrons, and Boltzmann scattering integrals for slow, equilibrium fraction of electrons.

The major differences between TREKIS-4 and XTANT are in the two main aspects: a) TREKIS-4 relies on the classical MD model, whereas XTANT uses tight-binding MD; b) TREKIS-4 has a much more advanced MC simulation module, accounting for many processes that are not included in XTANT. Point (a) allows TREKIS-4 to simulate much larger systems, with spatial dimensions that XTANT cannot cover. Point (b) makes TREKIS-4 more universal, allowing for modeling of a wide variety of incident radiation types and conditions (ions, electrons, positrons, photons, including relativistic energies) versus only X-ray photons in the nonrelativistic energy range in XTANT. On the other hand, since XTANT does not rely on the classical MD potentials, it is capable of tracing the evolution of the electronic structure and interatomic forces due to electronic excitation (such as nonthermal melting).\textsuperscript{[37]} Thus, the codes serve different purposes and are complementary to each other.

Below we describe all the details and parameters of the models implemented in TREKIS-4: the Monte Carlo method for each...
the integration limits are defined as follows [41].

\[ \lambda = -\lambda_0 \ln (\xi_1) \]  

(1)

here \( \xi_1 \in [0, 1) \) is a uniformly distributed random number, and the mean free path \( \lambda_0 \) is defined via a cross-section, \( \sigma \), as follows [39, 40]:

\[ \lambda_0^{-1} = \sigma n_{at} = n_{at} \int \frac{d^4\sigma}{dWdQ} dWdQ \]  

(2)

where \( n_{at} \) is the density of target atoms, \( \frac{d\sigma}{dWdQ} \) is the double differential cross-section, \( W_\text{e} \) and \( Q \) are the minimal and maximal transferred energy (W), and momentum in the energy units \( (Q(1 + Q(2m_i c^2)) = \frac{h^2}{2m_i} q^2/(2m_i) \), where \( q \) is the transferred momentum and \( m_i \) is the scattering center mass, \( h \) is the Planck constant, and \( c \) is the speed of light in a vacuum). [41] All masses used are the rest masses of particles.

For an incident particle with the kinetic energy \( E \) and mass \( M \), the integration limits are defined as follows [41]:

\[
\begin{aligned}
W_\text{e} & = \sqrt{E(E + 2Mc^2)} \frac{1}{2m_i c^2 E + (Mc^2 + m_i c^2)^2}, \\
Q_\text{e} & = \sqrt{\left(\sqrt{E(E + 2Mc^2)} - \sqrt{(E - W)(E - W + 2Mc^2)}\right)^2 + (m_i c^2)^2 - m_i c^2}
\end{aligned}
\]  

(3)

where \( I_p \) is the ionization potential of the atomic shell an electron is being ionized from in the case of inelastic scattering, and \( m_i \) is the mass of a target scattering particle. In the case of ionization from a valence band, \( I_p \) is \( E_{\text{gap}} \) (\( E_{\text{gap}} \) is the bandgap of the material). In the case of scattering on a conduction band electron, or elastic scattering on atoms, \( I_p = 0 \). In the case of identical particles scattering (electron–electron), \( W_\text{e} = (E + I_p)/2 \). [41]

In a scattering event, the sampled transferred energy, \( \delta E \), is also defined by the differential scattering cross-section according to the following expression [38]

\[ \xi_2 \sigma = \int_{W_\text{e}}^{Q_\text{e}} \frac{d^4\sigma}{dWdQ} dWdQ \]  

(4)

here \( \xi_2 \in [0, 1) \) is a different random number. Equation (4) is solved for the transferred energy \( \delta E \) with the bisection method (if an analytical solution is not available). Then, a particle deflection angle is calculated from the momentum conservation before subtracting ionization potential (in the case of inelastic scattering) [32]. The polar angle is chosen randomly within \( 2\pi \).

The following sections describe the specifics for each type of particle modeled and further simulation details.

### 2.1. Cross-Sections in the Linear Response Approximation

In the linear response approximation, the cross-section of a charged particle scattering reduces to the dependence on the longitudinal energy loss function—an imaginary part of the inverse complex dielectric function (CDF) of a target, \( \text{Im} [-1/\varepsilon(W, Q)] \) [42, 43]

\[
\left( \frac{d^4\sigma}{dWdQ} \right)_j = \frac{Z_2^2 Z_j^2}{\pi_e \alpha \beta} \left[ 1 - \exp \left( -\frac{W}{T} \right) \right]^{-1} \times \frac{2Mc^2}{WQ(Q + 2Mc^2)} \frac{W + mc^2}{mc^2} \text{Im} \left( \frac{-1}{\varepsilon(W, Q)} \right)
\]  

(5)

Here \( Z \) and \( Z_j \) are the charges of the incident particle and the target particle (scattering center), which will be discussed below for each type of particle, \( \alpha \) is the Bohr radius, \( \beta = v/c = \sqrt{1 - (1 + E/Mc^2)^{-2}} \) is the incident particle velocity normalized to the speed of light in a vacuum, \( m_i \) is the free-electron mass, \( T \) is the target temperature (in energy units).

In the ultra-relativistic case, a transverse part of CDF starts to contribute [15]. This contribution is currently neglected in TREKIS-4, which sets its upper limit of applicability at mildly relativistic energies [41].

With all the other parameters known, the problem reduces to the evaluation of the CDF. Here, we use the Ritchie–Howie formalism to obtain the CDF function parameters, approximated with the Drude–Lorentz oscillators form [44]

\[
\text{Im} \left( \frac{-1}{\varepsilon(W, Q)} \right)_{\text{RH}} = \sum_{j=1}^{N_{\text{osc}}} \frac{A_j y_j}{W^2 - (E_{0j} + Q)^2 + (y_j W)^2}
\]  

(6)

where \( y_j \) are the widths of the oscillators, \( E_{0j} \) define their positions, and \( A_j \) are their weights or contributions of target electrons into this oscillator. The set of parameters \( \{ y_j, E_{0j}, A_j \} \) for the number of oscillators, \( N_{\text{osc}} \), is fitted to reproduce available experimental or calculated optical parameters in the optical limit (\( Q = 0 \)) [42, 43].

It is known that in the case of proton transport, Ritchie–Howie oscillators in CDF do not produce sufficiently accurate energy losses [46, 47]. In this case, Mermin-like CDF oscillators can be used [46, 47]. It also may improve calculations of other particles’ mean free paths at low energies, if required. Mermin-like CDF uses the same input from the optical coefficients (optical limit, Equation (6)), but the extension from the optical limit to finite \( Q > 0 \) is done via Mermin dielectric function.
At high energies of a projectile, when \(|\gamma|<<\{W,Q\}\), the CDF may be reduced to a sum of the Dirac’s delta functions by formally setting \(\gamma \to 0\). \(^{41}\)

\[
\text{Im} \left( \frac{-1}{\varepsilon (W, Q)} \right) = \sum_{i=1}^{N_{\text{sp}}} \frac{a_i(0)}{W} \delta \left( W - (E_{i0} + Q) \right)
\]

(7)

where \(a_i(0) = \pi \lambda_i^2/2\) obtained from the same optical coefficients as Equation (6). Integration with the Dirac’s delta function alters the integration limits (Equation (3)) to more complicated expressions defined by Medvedev and Volkov\(^{41}\) which are, however, straightforward to implement into a numerical program.

Ritchie–Howie CDF coefficients for a number of solids can be found, e.g., in Ref. \([42]\). For other materials, one may construct CDF oscillators for a wide list of materials using optical coefficients\(^{48,49}\) (for low-energy photons) or databases\(^{50-53}\) (for high-energy photons), following the detailed instructions.\(^{54}\)

In an absence of optical parameters, the single-pole approximation may be used. In this case, Equation (6) is approximated with a single oscillator \(N_{\text{osc}} = 1\).\(^{55}\) The parameters of the CDF may then be approximated as follows. The position of the oscillator may be chosen according to the position of a collective mode of the oscillations of the particles: phonon mode for elastic scattering on the atomic system of a target (here approximated with the Einstein oscillation frequency, \(\omega_{\text{ph}}\)), or the plasmon mode for inelastic scattering on the valence/conduction band electronic system

\[
E_{\text{osc}} = \hbar \omega_{\text{ph}} = \pi \hbar c \sqrt{n_{e}}, \text{ elastic} \\
E_{0\text{sp}} = \max (\hbar p, l_p), \text{ inelastic}
\]

(8)

where \(c\) is the speed of sound in the material, and the plasmon frequency is defined as \(\omega_{\text{sp}} = \frac{2}{3} = 4\pi e^2 n_{e}/m_e\), with \(n_e\) being the valence/conduction band electron density. The choice of the maximum between the plasmon energy and ionization potential automatically identifies the plasmon energy for the valence/conduction band scattering, and ionization potential for core–shell scattering.

Within the single-pole approximation, the width of the CDF peak is currently empirically approximated as \(\gamma_{\text{sp}} = E_{0\text{sp}}/10\) for elastic scattering and \(\gamma_{\text{sp}} = E_{0\text{sp}}\) for inelastic one (which enter only in Equation (6) and vanish for delta-functional approximation, Equation (7)). The normalization coefficient is unambiguously defined by the \(k\)-sum rule\(^{56}\)

\[
A_{\text{sp}} = (\hbar p)^2 \int_0^\infty W \text{Im} \left( \frac{-1}{\varepsilon (W, Q = 0, A = 1)} \right) \frac{dW}{\varepsilon}
\]

(9)

This rather crude approximation allows evaluating the scattering cross-section and mean free paths of charged particles in complex materials, for which the optical coefficients are unknown.

To summarize, in TREKIS-4, the following cross-sections are used for the scattering of charged particles: wherever available, nonrelativistic inelastic scattering is described with Ritchie–Howie CDF, Equation (6), except for protons, for which Mermin-like CDF is used. For high-energy particles, delta-functional approximation (Equation (7)) is used. For materials, for which the optical coefficients are unavailable, the single-pole approximation with the parameters (8) and (9) is employed.

### 2.2. Ions

TREKIS-4 is capable of modeling ion impacts, from protons up to superheavy ions, in the regime of the electronic energy loss.\(^{57}\)

In this regime, the elastic (nuclear) scattering of a projectile is negligible, and only inelastic scattering is considered since it forms the main contribution to the ion energy loss \(S_i \gg S_e\), where \(S_i\) is the electronic energy loss, and \(S_e\) is the nuclear energy loss).\(^{42}\) Other processes such as radiation emission via Bremsstrahlung and Cherenkov emission are also negligible for ions since Bremsstrahlung is inversely proportional to the mass of a projectile.\(^{58}\) So, only the inelastic scattering of a projectile is considered, resulting in the impact ionization of electrons in target atoms or valence/conduction band.

To describe the inelastic scattering, cross-sections from Equations (1)–(5) are used, with the CDF models mentioned in the previous section. In the case of scattering on target electrons, the target mass and charge are set as free-electron parameters: \(m_e = m_e\), \(Z_i = 1\). The ion charge for protons is set \(Z = 1\), whereas for heavier particles (referred to as swift heavy ions, SHI), we use the Barkas approximation for the effective charge, \(Z = Z_{\text{eff}}(v)\).\(^{59}\)

\[
Z_{\text{eff}}(v) = Z_{\text{ion}} \left[ 1 - \exp \left( -\frac{v}{v_0} \right) \right]
\]

(10)

where \(v\) is the SHI velocity, \(v_0 = c/125\) is empirically adjusted atomic electron velocity,\(^{59}\) and \(Z_{\text{ion}}\) is the atomic number of the SHI in the Periodic Table. Such a simple approximation allows us to describe SHI energy loss across the entire energy range from a few MeV to TeV, without tracing complex charge exchange processes between the SHI and a target.\(^{41,62,68}\)

### 2.3. Electrons

Whether we are interested in an external electron impact on a target, or transport of secondary electrons excited by a projectile, modeling of electrons in a wide range of energies from a few eV up to MeVs must include at least the following processes: elastic and inelastic scattering. Bremsstrahlung photon emission, and boundary crossing with electron emission from the surface (if free surfaces are included in the simulation).\(^{15}\) For elastic and inelastic scattering, we use the linear response theory (Equations (1)–(7)), with the incident electron mass and charge set to free particle parameters \(M = m_e\), \(Z = 1\).

For inelastic scattering, the target mass and charge are also set as free-electron parameters: \(m_i = m_e\), \(Z_i = 1\). In an inelastic scattering event, a new electron is created, leaving a hole in a deep atomic shell, or the valence/conduction band of the material. The shell or band being ionized is chosen according to the partial ionization cross-section, normalized to the total one.\(^{40,42}\) In the case of the valence band ionization, the energy state, from which an electron is being excited, is chosen according to the unperturbed density of states (DOS) in the initial and final states of the material, for a given sampled transferred energy \(\delta E\).\(^{63}\) Then, the
transferred energy is subtracted from the incident electron energy, and the deflection angle is calculated.\textsuperscript{[16]} The electron being excited receives energy equal to the difference between the transferred energy and its ionization potential (or the energy state in the valence band plus the bandgap). Its momentum is defined from the energy and momentum conservation, calculated before subtraction of the ionization potential. In the initial state, target electrons are considered particles at rest.

For elastic scattering on target atoms, the CDF formalism takes into account that at low energies, an electron interacts with the collective modes of the atomic lattice – phonons, whereas at high energies it scatters on a frozen structure of atoms, reducing to scattering on isolated atoms with an increase of the electron velocity.\textsuperscript{[5,6,2,6,3]} Additionally, we take into account that with the increase of the electron velocity, the target atoms appear less and less screened by their own electrons. The effective charge of a target atom is set using the following approximation based on the Barkas effective charge (Equation (10))

$$Z_t = 1 + (Z_{a^{-1}}) \left[1 - \exp\left(-\frac{\nu}{\tau_{B}^{-1}}\right)\right]$$

(11)

$$Z_{a^{-1}} = Z_{a^{-1}} Z_t^{-1},$$

with $Z_t$ being the average atomic number of target atoms in a compound, and $\nu$ is the incident electron velocity. The rationale for the shape of Equation (11) is that the effective charge in elastic scattering of electrons on target atoms reduces to 1 for slow electrons, thereby restoring the known phononic limit,\textsuperscript{[64]} while for fast electrons, the effective charge reduces to the charge of an unscreened nucleus, reproducing the high-energy limit such as the Mott cross-section (screened Rutherford).\textsuperscript{[39,65]} Thus, Equation (11) produces a smooth connection between the two limiting cases within a unified approach. An example of such a calculated electron elastic scattering cross-section in SiO$_2$ is shown in Figure 1. The coefficients for the calculation of the CDF are obtained from Ref. [42].

After the scattering, the incident electron loses an amount of energy $\delta E$, calculated with Equation (4) with the elastic cross-section of scattering. This energy and coordinates of the scattering event are recorded for the bookkeeping as energy transfer to the target atoms (Section 2.7). The electron deflects accordingly to the energy loss and continues its transport.

For electron Bremsstrahlung emission we use Salvat and Fernandes-Vera expression, which extends and empirically adjusts the well-known Bethe–Heitler formula.\textsuperscript{[66]} All the parameters entering the formula are given by Salvat and Fern.\textsuperscript{[16]} In this scattering event, a photon is emitted, with energy sampled from the Bethe–Heitler differential cross-section according to Equation (4). Its energy is equal to the energy loss of the incident electron. Its direction of motion is chosen along the incident electron trajectory, with no deflection produced for the electron.\textsuperscript{[56]}

Material surface crossing and electron emission are modeled with an Eckart-type barrier.\textsuperscript{[67]} We neglect such effects as the scattering of excited electrons among themselves (free-free scattering), which limits the excited electron densities in the simulation to values below the densities of bound electrons. In this case, the impact ionization scattering is dominant, and free-free scattering may be neglected. We also do not account for long-range Coulomb interaction among the electrons and holes, which is also negligible for low excitation densities, close to quasi-neutral conditions, and especially for fast particles.\textsuperscript{[42]}

2.4. Holes

Holes left after impact ionizations or photoabsorption (considered below) will undergo their own kinetics, depending on the state they reside in. Core–shell holes will decay via Auger or radiative processes, emitting secondary particles. Holes in the valence band will behave like quasi-free particles, experiencing elastic and inelastic scattering events.

To model Auger and radiative decays of core holes, we use the exponential Poisson distribution of the lifetime

$$t = -t_0 \ln (\xi),$$

(12)

where $\xi \in [0, 1)$ is another random number, $t_0$ is the total decay time calculated according to the Matthiessen rule

$$t_0 = (1/t_{Au} + 1/t_{R})^{-1}$$

(13)

here $t_{Au}$ is the characteristic Auger decay time of the considered shell, and $t_{R}$ is its radiative decay time. Both are extracted from the EPICS2017 database (EADL part), which contains the characteristic decay times for each shell of each element across the Periodic Table.\textsuperscript{[52]} This database contains the data on ionization potentials of neutral atoms and decay times of single-ionized ions (not multiple-ionized ions). In the future, it is possible to improve it, accounting for multi-ionized states via, e.g., dedicated codes such as XATOM.\textsuperscript{[58]} A combination of XATOM with MD simulations has been performed in XMDYN as proof of the concept.\textsuperscript{[58]}

Having sampled the decay time for each hole, we identify those occurring within the current time-step of the simulation to perform the events. This procedure is repeated until all holes have decay-times longer than the current timestep.
The shells, participating in an Auger or radiative decay, are chosen according to probabilities from the EPICS2017 database.\(^{[52]}\) After an Auger decay, a new electron is emitted with energy equal to the difference between the binding energies of the involved shells. Its initial direction of motion is set randomly within a solid angle. The two new holes appear in the shells involved: one from which an electron fell to fill the decaying core hole, and another one an electron is emitted from.

The shell, into which a hole jumps during a radiative decay, is also chosen according to probabilities from EPICS2017.\(^{[52]}\) A photon is then emitted randomly within a solid angle, with the energy equal to the difference of the binding energies of the involved shells.\(^{[60]}\) The new holes will undergo their own decays analogously, until all holes created in a cascade end up in the valence/conduction band and cannot decay anymore.\(^{[42]}\)

The energy state of a hole in the valence band is chosen according to a probability proportional to the DOS.\(^{[60]}\) The kinetic energy of the hole is counted from the top of the valence band. The valence hole scattering is described with the same cross-sections (Equations (1)–(7)), with its own effective mass. The effective mass of a hole is obtained from the DOS using an effective one-band approximation.\(^{[40]}\)

Since holes are typically heavier than free electrons, their elastic scattering provides non-negligible energy to the atoms.\(^{[68]}\) Inelastic scattering of valence electrons is only possible in materials, where the width of the valence band is larger than its bandgap (such as semiconductors). In these events, a new electron is excited from the valence band into the conduction band, in the same manner as in the electron inelastic scattering.

Analogously to the electron transport, we neglect free-free scattering and long-range attraction or repulsion of holes.

### 2.5. Photons

Modeling of electromagnetic radiation in the terms of photons is significantly simpler within the MC method than in terms of fields. This photons-based approach is a standard one for description of radiation transport in matter for the case of X-rays or gamma-radiation. Albeit it neglects collective effects (which may be reduced to the limit of classical fields), for relatively small intensities/fluences considered here, treatment of individual photons is sufficient to describe the dominant effects.

Photons, either incident or created via core hole radiative decay or electron Bremsstrahlung, will experience their own scattering events. These are photoabsorption, elastic (Thomson or Rayleigh) scattering, inelastic (Compton) scattering, and electron–positron pair production.

Photoabsorption cross-sections for each core–shell of each element are extracted from EPICS2017 database (EPDL part).\(^{[32]}\) Photoabsorption length, \(\lambda_{\text{pa}}\), for absorption by valence/conduction band electrons is calculated from the CDF using the Fano relation\(^{[45]}\)

\[
\text{Im}\left(\frac{-1}{\varepsilon(a, 0)}\right) = \frac{c}{\alpha \lambda_{\text{pa}}}
\]  

(14)

In a photoabsorption event, a photon disappears, and an electron is emitted with energy \(E = \hbar \omega - I_p\). Its polar angle is set randomly within the \(2\pi\) interval. Its azimuth angle is set using the standard Sauter kernel,\(^{[16]}\) which makes a uniform electron emission for low-energy photons and a preferential forward direction for relativistic energies.

Elastic, also called coherent, scattering is calculated using the Rayleigh expression.\(^{[16]}\) It includes a classical Thomson scattering cross-section modified by the atomic form factor of the target atom. Rayleigh scattering disregards anomalous scattering factors in the current model. In such a scattering, a photon changes its direction of motion without changing its energy.

The Compton scattering event is similar to the Rayleigh scattering, but a photon loses some energy in the scattering event, thereby emitting an electron from a target atom. It is also known as incoherent scattering.\(^{[16]}\) We use the standard Klein–Nishina formula for the evaluation of the Compton scattering cross-section.\(^{[16]}\) Only electron transitions to a free state (ionization) are allowed in such a process. Electron energy and azimuthal emission angle are sampled from the differential cross-section.\(^{[16]}\) The polar angle is set randomly within the \(2\pi\) interval.

Electron–positron pair production for high-energy photons is calculated according to the Bethe–Heitler model.\(^{[16]}\) The screening functions and correction terms are taken from the PENLOPE model.\(^{[16]}\) This process only occurs for photon energies \(\hbar \omega > 2m_e c^2\), which does not realize in the cases we discuss in the present work.

### 2.6. Target Atoms

To trace the response of the target atoms to deposited energy, we use the molecular dynamics (MD) method with the velocity Verlet integration algorithm.\(^{[69]}\) Periodic boundary conditions are used for atoms in the simulation box, assuming a bulk target (no free surfaces). Depending on the symmetry of the problem, appropriate parts of the simulation cell may be cooled down with the Berendsen thermostat\(^{[70]}\)

\[
T(t + \delta t) = T_0 + \left(T(t) - T_0\right) \exp(-\delta t / \tau)
\]  

(15)

where \(T(t + \delta t)\) and \(T(t)\) is the atomic temperature on the current and previous time step (before and after cooling), \(T_0\) is the bath temperature (typically, room temperature, 300 K), \(\tau\) is the characteristic cooling time, and \(\delta t\) is the MD time step. Note that Equation (15) is an exact solution of the equation for the temperature rate, in contrast to the linearized one in the original work,\(^{[70]}\) and thus it does not require the condition \(\tau \gg \delta t\).

For simulation of localized ion tracks, the borders of the simulation box are cooled with the Berendsen thermostat.\(^{[17]}\) This allows mimicking the realistic scenario of a track embedded in an unirradiated target using a finite-size supercell. For laser pulse simulations, an entire supercell may be homogeneously cooled at a slower rate, or no cooling at all may be used.\(^{[71]}\)

In this work, to simulate \(\text{Al}_2\text{O}_3\), we apply Matsui potential, which is a Buckingham-type potential with a Coulomb term.\(^{[71]}\) For evaluation of the Coulomb interaction, we apply Wolf’s method of truncation in its energy-conserving form.\(^{[72]}\)

The initial conditions for atoms are set as a perfect crystalline structure with the random velocities assigned to atoms with the Maxwellian distribution (at room temperature). The atoms are
allowed to equilibrate for a few hundred femtoseconds prior to the arrival of radiation. The energy transfer from the excited electronic system (modeled with MC as described above) to the MD atoms is described in the next section. Atoms receive this transferred energy at each time step of the simulation via velocity scaling. Atomic snapshots illustrations are prepared with help of VMD software.[73]

2.7. Energy Exchange

We account for three mechanisms of energy transfer between excited electrons and atoms: elastic scattering of electrons, holes, and nonthermal heating of atoms. The energy transferred in elastic scattering of electrons and holes, recorded in each scattering event as described in the previous sections, is averaged over all MC iterations on each time step of concurrent MC–MD simulations. It forms a continuous spatial distribution of energy to be fed to atoms.

As was discussed by Medvedev and Volkov[74] (based on the theoretical[37,75,76] and experimental results[8,77,78]), nonthermal effects quickly convert potential energy built up due to electronic changes of the interatomic potential into kinetic energy of atoms. The modifications of the interatomic potential due to electronic excitation are not straightforward to include in a classical MD.[58] Although it is in principle possible to use electronic-temperature-dependent interatomic potentials, in practice, they are only available for a limited number of solids[18] and are tricky to implement.[79] In the current implementation of TREKIS-4, we use a different approach.

Taking into account the empirically tested idea of approximating this energy conversion as the bandgap energy from each created valence hole,[28] we set the following procedure. When a valence hole in the simulation loses its energy below a chosen cut-off, its remaining kinetic energy and the potential energy equal to the bandgap of the material \(E_{\text{cut}} = 8.8 \text{ eV for Al}_2\text{O}_3\) are added as the energy transferred to atoms. In this process, electrons and holes with energy dropped below the cut-off disappear from the MC simulation (considered “stopped”). The cut-off is set as \(E_{\text{cut}} = 0.1 \text{ eV}\), which produces a reasonable speed of atomic heating in comparison with the ab initio-based simulations. The modification of the interatomic potential and ensuing increase of the kinetic energy of atoms, as will be shown below.[74] The value of \(E_{\text{cut}}\) is chosen once from a comparison with XTANT, reported in the next section, and serves as a universal parameter for all further simulations.

The spatial distribution of energy lost by electrons and holes in the elastic scattering and the energy transferred when electrons and holes stop (reach the energy cut off) are averaged over all concurrently executed MC iterations at the current time step. The averaged energy distribution may be recorded in zero, one, two, or three dimensions, in Cartesian, spherical, or cylindrical coordinates, depending on the problem at hand. The energy within each subcell defined on the given grid is then distributed to atoms in MD located within the same subcell. We use a simple velocity scaling algorithm to deliver energy to atoms, which conserves the total momentum in the simulation box. More advanced methods such as the Langevin thermostat may be implemented in the future.[80]

The MD simulation box covers a smaller region in space than the MC grid for excited particles transport. Only the energy inside the MD box is delivered to atoms for further simulation; the energy outside of the MD box is stored for bookkeeping, to test the total energy conservation in the simulation scheme.[36]

3. Results

Below we consider two examples. The first one is irradiation of alumina with femtosecond soft X-ray laser pulse, which will allow us to validate the developed model via comparison with previously published results.[81] After validation of the model, we will consider irradiation of alumina with a swift heavy ion to gain new insights into the processes that could not have been studied before without a hybrid model resolving electronic and atomic kinetics simultaneously.

3.1. X-Ray Pulse Irradiation of \text{Al}_2\text{O}_3

To validate the proposed combined approach, we modeled irradiation of \text{Al}_2\text{O}_3 with a femtosecond soft X-ray laser pulse: 92 eV photon energy, 10 fs full width at half maximum (FWHM) Gaussian temporal profile, and 2 eV per atom absorbed dose. Since the laser spot is typically of a few micrometer size, much larger than the simulation box, we assume homogeneous irradiation of the supercell. The depth profile of the photoabsorption is defined by the Lambert–Beer law. The number of photons is defined by the chosen absorbed dose, from the condition that the total number of absorbed photons would deliver the chosen total energy into the simulation box. The time of each photon arrival is sampled according to the Gaussian function with the defined FWHM.

To compare the results with previously published ones,[81] no thermostats were used, assuming the NVE ensemble of atoms. All MC particles were locked within the simulation box equal in size to the MD simulation box with periodic boundary conditions. 1000 MC iterations are used to obtain reliable statistics. The simulation box contained 18 000 atoms in the TREKIS-4 simulation; the simulation box of 240 atoms was used due to computational resources consumption of the tight-binding MD of XTANT-3 code.[81]

Applied irradiation excites initially the sample electronic system, which then deposits a part of the excess energy into the atomic one. Figure 2a shows the increase in atomic energy due to this energy transfer. The initial increase of the total atomic energy during the first \(\approx 50\) fs takes place due to interaction with the primary electron cascades, whereas the long tail is formed by Auger-electrons, released from the L-shell of Al, decaying with the characteristic time of \(\approx 110\) fs.[52] Figure 2a shows that the results of XTANT-3 and TREKIS-4 simulations coincide well, validating the coupling of the MC and MD modules, responsible for the energy exchange between the electronic and the atomic systems.

Figure 2b shows the increase of the kinetic energy of atoms mainly via nonthermal heating in XTANT-3.[74] The agreement between XTANT-3 and TREKIS-4 results demonstrates that the proposed “hole termination” approximation for the conversion of the electronic excitation due to transient changes in the interatomic potential into the increase of kinetic energy of atoms captures this effect with good accuracy (see Section 2.7). Larger
oscillations in XTANT-3 results are due to finite size effects of the significantly smaller simulation box. The agreement validates the proposed simple scheme incorporating the nonthermal heating effects within a combined MC and classical MD simulations.

### 3.2. Swift Heavy Ion Irradiation of Al₂O₃

To simulate a swift heavy ion impact, we use Xe ion with the incident energy of 30 MeV. Cylindrical coordinates were applied to trace energy deposition from MC particles to MD atoms. The transferred energy was traced on a radial grid with the step of 3 Å. Periodic boundary conditions for MC particles were set at the Z coordinate, along which the SHI was traversing once, with no boundaries along other coordinates allowing particles to travel freely. The MD simulation box containing 54 000 atoms (size 12.56 × 14.5 × 2.6 nm) was used with periodic boundary conditions along all axes, and with the Berendsen thermostat acting within 5 Å border layers along the X and Y axes. The characteristic cooling time of 10 fs was used. The size of the supercell was limited due to computational demands: the thickness of 2.6 nm allows for treating sufficiently large dimensions along the X and Y axes, which is important to model spatial propagation of excitation around an ion track. Changing the supercell size should not affect the results as long as the size is significantly smaller than the characteristic length at which SHI energy changes noticeably. Typically, it means simulation boxes of a size <50–100 nm. For typical energies of swift heavy ions considered, they pass the distance of 2.6 nm within the time of ≈10 as. So, within sub-femtosecond timescales, the image of the simulation box “below” experiences the same excitation as the one “above,” rendering the problem homogeneous along the Z-axis (trajectory of ion penetration). This is a standard approximation for the SHI beam problem. Changing the size of the simulation box does not affect the results, since a typical ion range is on the order of nm—much larger than the dimensions of the simulation box.

The average integral energy redistribution among various systems after an impact of Xe (30 MeV) in alumina modeled with TREKIS-4 is shown in Figure 3. This figure confirms overall energy conservation in the simulation scheme. It shows that the energy is primarily deposited by the ion to the electronic system, where holes initially possess ≈50% of the energy, in agreement with the literature.⁶⁸,⁸² Electrons quickly lose their energy into the atomic system via both energy channels, elastic scattering, and energy transfer when they “stop”—when their energy drops below the cut-off. Core holes transiently accumulate a significant amount of potential energy. They decay predominantly via the Auger decay channel, as can be seen from a negligible amount of energy stored in photons emitted via radiative decays. When holes cascade are over, they end up in the valence band. Then, they release the energy into the atomic system (transferring it into the MD module) in the same manner as electrons. We see that in the case of an SHI impact, almost all the energy is transferred to atoms already within sub-100 fs timescales, also in agreement with previous studies.¹⁷,²⁸

The spatial distribution of the energy transfer rate from the electronic to the atomic system is shown in Figure 4. The radial distribution decays exponentially, but its shape is not constant in time. Moreover, different channels are dominant at different times. Initially, at the time of ≈1 fs, the energy transfer is mostly
Figure 4. The energy transfer rate from electronic (modeled with MC) to atomic (modeled with MD) system, simulated with TREKIS-4 for Al$_2$O$_3$ irradiated with Xe (30 MeV) ion at different time instants.

from the elastic scattering of fast electrons close to the ion trajectory. Later at ≈10 fs, electrons scatter and escape outward from the center, and form a dominant contribution at larger radii. After that, electron cascades are nearly over in the proximity of the SHI trajectory—they mainly continue at large radii, not shown in Figure 4 (outside of the boundaries of the MD simulation box). Potential energy transfer (via bandgap energy as the potential energy of valence holes, see model in Section 2.7) dominates later after ≈10 fs. Elastic scattering of valence holes makes a small but not negligible contribution too. Since the behavior of electrons and holes is different, these sources of energy transfer to the atomic system cannot be reliably traced with a single equation for the electronic system such as the thermodiffusion equation used in TTM–MD.[31,33,83]

Atomic snapshots shown in Figure 5 illustrate the atomic response to this energy deposition. A cylindrical track of disordered material forms around the SHI trajectory. By the time of ≈50 fs, the electron cascades are nearly over (Figure 3), whereas atomic disorder is just starting (cf. Figure 5). Note that the atomic disorder takes place at the timescale of a few hundred fs, much faster than the electron–phonon coupling would have heated atoms up. This atomic heating is a result of the effects of elastic scatterings of electrons as well as valence holes, which do not involve phonons,[43,52,63] and important nonthermal atomic heating via conversion of the changes of the potential energy of atoms into their kinetic energy.[74] All three mechanisms of the energy exchange are different from the electron–phonon coupling. They cannot be captured with the formalism of the two-temperature model, which resulted in the need to use adjustable parameters in TTM–MD models of SHI track creation.[31,33,83]

The formation of a track in Figure 5 agrees well with previously reported simulations,[28] as discussed in more detail in the Appendix. The results become nearly identical after ≈100 fs, which proves that the model of an instantaneous energy deposition used by Rybnikov et al.[28] produces reasonable results for the final track formation. However, models that use electron energy transfer as initial conditions for MD,[28] are missing the stage of the energy deposition into the atomic system, when the simultaneous kinetics of excited electronic system and atomic lattice response occur.
4. Discussion

Our results show that after ultrashort energy deposition into the electron system, the electronic kinetics for the most part proceeds in an unchanged atomic system. Atoms react to the energy deposition from the electrons and holes at timescales longer than those of relaxation of the electronic system. A similar notion was discussed in the case of a femtosecond X-ray irradiation before.[84] This suggests that a model, where output data of an MC simulation are used as input data for the MD simulation of atomic response, often suffices to describe the target kinetics (see the Appendix for more details). It is a good approximation in the case of ultrafast energy deposition and short-lived secondary electron cascades. In this case, atomic reaction mainly takes place after the electronic kinetics is over, which means that the electronic processes mainly occur in a still unchanged material. This approximation was used in earlier works as an apriori assumption,[26,28,85] which could not have been confirmed without a hybrid simulation such as the one implemented in this work.

In the current implementation, the electrons in MC are not sensitive to the state of the atomic system. For example, atomic velocities and coordinates do not affect electron scattering. It is possible to include feedback from the atomic system to the electronic one in multiple ways. For instance, Equations (6) and (7) do not account for changes in the CDF with a change in material temperature and structure. The temperature factor in the cross-section (Equation (5)) only accounts for a part of the temperature dependence.[86] For the studied cases, it is a sufficient approximation, since the cascades proceed mostly in an unirradiated part of the sample, and are over when the material properties change noticeably.[13,84] For future developments and applications of longer irradiation pulses (such as picosecond X-ray laser pulses, intensive electron or ion beams), it will be important to account for the ongoing evolution of the CDF during the target response. For example, a synergy effect of fast changes of the potential field for the atomic system with its temporal heating can considerably change the electron-ion coupling parameter governing lattice excitation.[74] For that, one may consider models used in plasma physics, such as Lindhard,[87] Mermin,[88] or full-conserving CDF.[89]

One should also bear in mind that the proposed algorithm only passes average data between MC and MD. This means rare fluctuations far from the mean are neglected. They could, potentially, lead to unusual states that are unaccounted for. Since the calculations are typically compared with experiments that also average over statistics of many-particle impacts/laser shots, we consider it a sufficient approximation at present.

To model the final material state, MC data may even be used as initial conditions for MD, without time resolution, as was done in previous works.[17,26,28,85] Such one-way information passage significantly simplifies the application of the respective models, but loses information on the initial stage of atomic dynamics and thus is unsuitable to describe time-resolved experiments.[90] The current state of the art of time-resolved ion beam experiments has a resolution of some ≈500 fs,[91] which is insufficient to resolve this stage. Further advances in future experiments with improved time resolution should be able to resolve it. For that, it will be crucial to describe the stage of electron-lattice energy exchange with an appropriate model, as proposed in this work. Current FEL pulses and electron diffraction experiments already have sufficient time resolution to probe this state.[77,92,93] The proposed model can be useful for such applications.

The model of conversion of the potential energy of electron-hole pairs into the kinetic energy of atoms that uses the bandgap energy (Section 2.7) applies to materials where the bandgap fully collapses upon high electronic excitation. It is primarily covalently bonded materials, whereas ionic materials may experience only partial bandgap collapse.[94] In such a case, the energy release must be modified to correspond to the bandgap shrinkage, estimated with help of ab initio simulations. In metallic targets, nonthermal effects manifest differently and
may be accounted for, e.g., via so-called electron blast force\textsuperscript{95} or electronic pressure.\textsuperscript{96} For metals, it may also be necessary to include an additional model for conduction band electrons, such as a thermo- or hydrodynamical approach.\textsuperscript{85}

We have to point out a limitation of the model connected with the fact that semiempirical MD potential was used in TREKIS-4. The tight-binding MD in XTANT-3 predicted a transient formation of a superionic state in fs-X-ray-laser irradiated Al\textsubscript{2}O\textsubscript{3},\textsuperscript{81} which was supported by the DFT-MD simulations.\textsuperscript{97}

In this state, oxygen sublattice melts, whereas aluminum one stays crystalline. TREKIS-4 simulation was unable to reproduce this phase because the MD potential used was constructed for the ground state of the electronic system, and thus cannot capture the effects of the modifications of the potential due to electronic excitation.\textsuperscript{18} It is, however, a general problem of classical MD simulations, not specific to TREKIS-4. It may, in principle, be remedied by using electronic-temperature-dependent potentials,\textsuperscript{98,99} but we know of none available for Al\textsubscript{2}O\textsubscript{3}.

Another limitation of the model is the fact that the linear response approximation (Equation (5)) relies on the first-order Born approximation.\textsuperscript{43,62} Strictly speaking, it limits its applicability to electron energies above some $\approx 50$ eV (and for heavier particles, to energies rescaled by the mass ratio correspondingly). At lower energies, further improvements are necessary. However, for high-energy particle impacts, the contribution of scattering at such low energies is rather small. For swift heavy ions, the error at energies below the Bragg peak is compensated to some degree by the usage of the effective charge, Equation (10).

5. Conclusion

We conclude that the reported simulation scheme of irradiation of nonmetallic materials combining Monte Carlo with molecular dynamics on-the-fly presents a viable extension to or a replacement of the standard approaches such as TTM–MD. An MC–MD combination allows accounting for nonequilibrium processes in the electronic system and their effects on the atomic dynamics. It also includes ballistic transport of various types of particles (electrons, valence holes, photons). It is straightforward to construct additional models in the same spirit to cover larger spatial or longer temporal scales, if necessary.

We proposed a simple model to account for the nonthermal energy exchange between electrons and atoms in covalent materials via conversion of the potential energy of electron–hole pairs into kinetic energy of atoms on-the-fly. The advantage of such an approach is that it can readily be implemented into standard MC models, without complex ab initio simulations of the effect. A comparison of the results obtained for a femtosecond X-ray pulse irradiation with Monte Carlo tight-binding MD simulations validated the model to a reasonable accuracy. Application of the developed MC–MD model to Al\textsubscript{2}O\textsubscript{3} allowed us to study the atomic heating stage after a swift heavy ion impact.

Our analysis suggests that even one-way information passage from MC modeling of the electronic system to MD modeling of the atomic one may suffice in many cases, such as ultrafast energy deposition and short electron cascades (when electronic processes finish before significant changes in the atomic system take place). It is a typical case of swift heavy ion or femtosecond laser pulses irradiation. Using properly recorded MC output as initial conditions for MD would work well for the purposes of tracing postmortem material damage, but not for a description of time-resolved experiments.

**Appendix**

Figure 6 shows a comparison of the results within the first 100 fs of irradiation of Al\textsubscript{2}O\textsubscript{3} with 30 MeV Xe ion simulated with the proposed TREKIS-4 approach versus previous results of combined MC output data on atomic
heating from TREKIS-3 as an instantaneous input for an MD simulation with LAMMPS. The difference appears only during the stage of energy exchange between the electrons and atoms: TREKIS-4 demonstrates a smaller transient track while the energy is still being transferred to atoms versus a larger track simulated with TREKIS-3 + LAMMPS. However, by the time electron cascades and energy transfer are finished ($\leq 100$ fs), the simulated tracks become nearly identical. Slightly larger size in the TREKIS-4 simulation at 100 fs is attributed to the used elastic scattering cross-section with the effective charge of target atoms, Equation (11), whereas TREKIS-3 used $Z_e = 1$ (phononic limit).

Further relaxation is identical in both cases since it is modeled with a classical MD with the same interatomic potential. Thus, it supports our conclusion that the final size of an SHI track may be reliably calculated with the model using appropriate initial conditions. Whereas for the description of time-resolved kinetics, the proposed methodology (implemented in TREKIS-4) may be used to cover the stage where electronic and atomic dynamics overlap.

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Conflict of Interest

The authors declare no conflict of interest.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

free-electron lasers, hybrid model, molecular dynamics, Monte Carlo, non-thermal melting, swift heavy ion track

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