Inferring *Plasmodium vivax* Transmission Networks from Tempo-Spatial Surveillance Data

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**Abstract**

**Background:** The transmission networks of *Plasmodium vivax* characterize how the parasite transmits from one location to another, which are informative and insightful for public health policy makers to accurately predict the patterns of its geographical spread. However, such networks are not apparent from surveillance data because *P. vivax* transmission can be affected by many factors, such as the biological characteristics of mosquitoes and the mobility of human beings. Here, we pay special attention to the problem of how to infer the underlying transmission networks of *P. vivax* based on available tempo-spatial patterns of reported cases.

**Methodology:** We first define a spatial transmission model, which involves representing both the heterogeneous transmission potential of *P. vivax* at individual locations and the mobility of infected populations among different locations. Based on the proposed transmission model, we further introduce a recurrent neural network model to infer the transmission networks from surveillance data. Specifically, in this model, we take into account multiple real-world factors, including the length of *P. vivax* incubation period, the impact of malaria control at different locations, and the total number of imported cases.

**Principal Findings:** We implement our proposed models by focusing on the *P. vivax* transmission among 62 towns in Yunnan province, People’s Republic of China, which have been experiencing high malaria transmission in the past years. By conducting scenario analysis with respect to different numbers of imported cases, we can (i) infer the underlying *P. vivax* transmission networks, (ii) estimate the number of imported cases for each individual town, and (iii) quantify the roles of individual towns in the geographical spread of *P. vivax*.

**Conclusion:** The demonstrated models have presented a general means for inferring the underlying transmission networks from surveillance data. The inferred networks will offer new insights into how to improve the predictability of *P. vivax* transmission.

**Introduction**

As one of the malaria parasites that can infect and be transmitted by human beings, *Plasmodium vivax* has induced enormous challenges to the public health of human population. It has been estimated that 2.5 billion people all over the world are at risk of infection with this organism, among which China accounts for 19% of the global populations at risk [1]. To control, eliminate or even eradicate malaria, WHO has suggested that the most important measure is a timely response with the implementation of strategic intervention [2]. This requires the establishment of effective and efficient monitoring or surveillance systems [3]. Moreover, in practice, human mobility can introduce malaria into previously low-transmission or malaria-free areas, which has been cited amongst the significant causes of the failure of the Global Malaria Eradication Programme [4]. Therefore, it would be desirable to investigate the underlying geographical spread of malaria, which is not apparent from surveillance data. In this paper, the transmission networks of *P. vivax* characterize how the parasite transmits from one geographical location to another due to human mobility. By focusing on the malaria transmission in Yunnan province, People’s Republic of China, we pay special attention to the problem of how to infer the underlying transmission networks of *P. vivax* based on tempo-spatial patterns of observed/reported cases.

Natural transmission of *P. vivax* depends on the interactions between female anopheles mosquitoes and human beings. On the one hand, the ability of mosquitoes to transmit *P. vivax* within a geographical location is dependent upon a series of biological factors, such as the daily survival rate of mosquitoes and the
The transmission of *Plasmodium vivax* has induced enormous public health problems at the global level. Natural transmission of *P. vivax* depends on interactions between anophelines mosquitoes and human beings. There are two important factors that influence its geographical spread. First, different locations may have different risks of infection due to their heterogeneous environmental and demographic profiles. Second, human mobility may bring pathogens from high-transmission locations to low-transmission locations. In view of this, to effectively and efficiently control the geographical spread of *P. vivax*, it would be desirable for us to characterize how it transmits from one location to another. To achieve this, we first build a spatial transmission model to characterize both the heterogeneous infection risks at individual locations and the underlying mobility of infected populations. By doing so, we can further infer the underlying *P. vivax* transmission networks from tempo-spatial surveillance data by using a machine learning method (i.e., based on a recurrent neural network model). Our study offers new insights into malaria surveillance and control from the viewpoint of both system modeling and machine learning.

Author Summary

The transmission of *Plasmodium vivax* has induced enormous public health problems at the global level. Natural transmission of *P. vivax* depends on interactions between anophelines mosquitoes and human beings. There are two important factors that influence its geographical spread. First, different locations may have different risks of infection due to their heterogeneous environmental and demographic profiles. Second, human mobility may bring pathogens from high-transmission locations to low-transmission locations. In view of this, to effectively and efficiently control the geographical spread of *P. vivax*, it would be desirable for us to characterize how it transmits from one location to another. To achieve this, we first build a spatial transmission model to characterize both the heterogeneous infection risks at individual locations and the underlying mobility of infected populations. By doing so, we can further infer the underlying *P. vivax* transmission networks from tempo-spatial surveillance data by using a machine learning method (i.e., based on a recurrent neural network model). Our study offers new insights into malaria surveillance and control from the viewpoint of both system modeling and machine learning.

Materials and Methods

A spatial transmission model

Due to the complex nature of *P. vivax* transmission, to infer the underlying transmission networks, appropriate spatial transmission model should first be formulated. In this paper, we aggregate the tempo-spatial series of surveillance data for each individual town based on a time step with duration $\Delta t$. In reality, $\Delta t$ may be different.
related to the incubation period of malaria (i.e., the period from the point of infection to the appearance of symptoms of the disease). In doing so, we assume that the observed/reported infections at time step \( t + 1 \) are more likely to be infected at previous time step \( t \). Generally speaking, the causes of geographical spread of \( P. \) vivax are twofold. First, within a town/node \( v_i \), the number of malaria infections \( y_i(t) \) at a time step \( t \) is determined by multiple factors, such as temperature, rainfall, population size, as well as the number of infections \( y_i(t-1) \) at previous time step \( t-1 \). Second, human mobility may introduce \( P. \) vivax from one town to another. Specifically, we focus mainly on the mobility of infected populations among different towns because patients with typical malaria symptoms will be rapidly diagnosed and treated in Yunnan, P.R. China. It is seldom for a diagnosed patient to cause further malaria infection.

### Malaria transmission potential at the nodal level

To model \( P. \) vivax transmission at a node, we use the notion of vectorial capacity \((\text{VCAP})\), which is defined as “the number of potentially infective contacts an individual person makes, through vector population, per unit time [13].” The \( \text{VCAP} \) is adapted from the basic reproductive number calculated based on the Macdonald model [14]. At each node \( v_i \in V \), the value of \( \text{VCAP} \) is given by:

\[
\text{VCAP}_i(t) = \frac{-m_i a_i^n_i}{\ln(p_i)},
\]

where \( m_i \) represents the equilibrium mosquito density per person, \( a_i \) is the expected number of bites on human beings per mosquito per day, \( p_i \) is the probability of a mosquito surviving through one whole day, and \( n_i \) is the entomological incubation period of malaria parasites. Based on the study of Ceccato et al. [6], all these parameters are dynamically dependent on temperature \((T)\) and rainfall \((R)\) at node \( v_i \). Table 2 shows the detailed parameter descriptions and settings in this work for calculating the vectorial capacity of each individual town in Yunnan. It should be noted that the values of relevant parameters are based on a certain degree of assumptions and estimates, and they could be adjusted once more accurate values are available in the future.

To further estimate the number of infections at a node \( v_i \), we introduce another notion of entomological incubation rate \((\text{EIR})\), which is defined as the number of infectious bites received per day by a human being [15]. Let \( x_i(t) \) denote the proportion of infected populations among all human populations at \( v_i \) at time step \( t \), i.e., \( x_i(t) = y_i(t)/P_i \). Here, \( y_i(t) \) is the number of observed/reported infections at \( v_i \) at time step \( t \), and \( P_i \) is the population size of \( v_i \). Figure 4 shows a schematic diagram illustrating various data sources utilized (i.e., physiological, environmental, demographical, and surveillance data) for characterizing the infection risks of \( P. \) vivax at each individual town based on the notion of EIR. Mathematically, \( \text{EIR}(t) \) can be calculated through \( V_i(t) \) as follows:

\[
\text{EIR}_i(t) = \frac{c \cdot V_i(t) \cdot x_i(t)}{1 + c \cdot a_i(t) x_i(t)/g_i(t)},
\]

where \( c \) denotes the probability of the disease transmitting from an infectious person to an uninfected mosquito, \( g_i(t) = -\ln(p_i(t)) \) represents the daily death rate of a mosquito [15].

Based on the definition of \( \text{EIR} \), the estimated number of infections without considering human mobility at time step \( t + 1 \) can be estimated as follows:
where \( b \) represents the probability of the disease transmitting from an infectious mosquito to an uninfected person, and \( b_i \) represents control impact of malaria transmission at node \( v_i \). Here, the control impact \( b_i \) measures the efficiency of various intervention strategies implemented at node \( v_i \), such as insecticide treated nets, and long-lasting insecticide-treated nets. Although according to Equation 3, the estimated number of human infections at \( t_z \) is a linear function of \( EIR \) at \( t \), the nonlinear interactions of infected mosquitoes and susceptible human beings and vice versa are taken into account in Equations 1 and 2 associated with \( VCAP \) and \( EIR \), respectively. Specifically in this paper, since all of the 62 towns are within Yunnan, we assume the malaria control strategies over them have the same impact. Without loss of generality, we can set \( b_i = c = 1 \), which corresponds to perfect malaria transmission between human beings and mosquitoes. In reality, these parameters can be estimated by assessing biting habits of mosquitoes at different locations and conducting virological and serological analysis on infected individuals [16–18].

The mobility of infected populations at the network level. In the following, we introduce how to model the mobility of infected populations with respect to the geographical spread of \( P. vivax \). Since human mobility among the 62 towns in Yunnan mainly relies on road transportation, in this paper, we assume that the transmission networks of \( P. vivax \) have the same topology (i.e., connectivity) with the transportation network. By doing so, we can quantify the transmission of \( P. vivax \) from one node to another by learning the link weight \( w_{ij} \) between them, which stands for the proportion of infected populations moving from \( v_i \) to \( v_j \) [Note that in this paper, the weight only characterizes the mobility of infected populations, where the population size of each node indirectly contributes to the weight via \( EIR \). Accordingly, taking into consideration the mobility of infected populations, the number of increased infections at node \( v_i \) can be calculated as follows:

\[
\delta_i(t+1) = b_i - P_i \cdot b_i \cdot EIR_i(t), \tag{3}
\]

\[
\Delta_i(t+1) = \sum_{v_j \notin \mathcal{N}(v_i)} \delta_i(t+1)w_{ij} - \sum_{v_k \in \mathcal{N}(v_i)} \delta_i(t+1)w_{ik}, \tag{4}
\]

which represents the difference between the number of cases transmitted from neighboring nodes and the number of cases transmitted to neighboring nodes. In summary, the estimated number of new infections of node \( v_i \) at time step \( t+1 \) should be:

\[
o_i(t+1) = \delta_i(t+1) + \Delta_i(t+1), \tag{5}
\]

A recurrent neural network model

After modeling the spatial transmission of \( P. vivax \), we further introduce a recurrent neural network model, which allows for

\[
\delta_i(t+1) = b_i - P_i \cdot b_i \cdot EIR_i(t), \tag{3}
\]

\[
\Delta_i(t+1) = \sum_{v_j \notin \mathcal{N}(v_i)} \delta_i(t+1)w_{ij} - \sum_{v_k \in \mathcal{N}(v_i)} \delta_i(t+1)w_{ik}, \tag{4}
\]

\[
o_i(t+1) = \delta_i(t+1) + \Delta_i(t+1), \tag{5}
\]
reflecting both structural (or spatial) and temporal dependencies of
the nodes in the network by creating interdependent internal
states in the model [19]. Specifically, we build the model by
taking into consideration the control impact at individual nodes,
the road transportation network, as well as the total number of
imported cases to the

\[ N \]
towns from the outside. Figure 5
illustrates the internal states of the model within a time step.
There are totally \( sd \) hidden layers in the network, and the links
between two hidden layers are determined by the connectivity of
the transportation network. Each hidden layer describes one stage
of disease transmission between two neighboring towns. In doing
so, to guarantee the possibility that one infected person may
travel to any other towns at a time step, \( sd \) should be equal to the
diameter of the road transportation network. The diameter of a
network refers to the greatest distance between any pair of nodes
in the network. To reflect the impact of

\( P. \) vivax
control at

\( \beta \)
individual nodes, a vector \( \beta = \langle \beta_1, \cdots, \beta_N \rangle \) is associated to the
out-links of the nodes in the input layer. In addition, the total
number of imported cases (i.e., \( Z(t) \)) of all the \( N \) towns is linked
to the \( N \) nodes in the output layer of the neural network, where a
vector \( \gamma = \langle \gamma_1, \cdots, \gamma_N \rangle \) \( (\sum_{i=1}^{N} \gamma_i = 1) \) is associated with \( Z(t) \) to
represent the proportion of imported cases each town received in
all the imported cases.

Table 1. The IDs and names of the studied 62 towns in
Yunnan, P.R. China.

| ID | Name   | ID | Name   | ID | Name   | ID | Name   |
|----|--------|----|--------|----|--------|----|--------|
| 1  | Shangying | 17 | Mangbang | 33 | Mengnong | 49 | Mangzhan |
| 2  | Zhonghe  | 18 | Hehua   | 34 | Kachang  | 50 | Nabin   |
| 3  | Wuhe     | 19 | Puchuan | 35 | Taiping  | 51 | Tongbigan |
| 4  | Menglian | 20 | Mazhan  | 36 | Jiemao   | 52 | Mengyue |
| 5  | Beihai   | 21 | Mengnuo | 37 | Gangmeng | 53 | Chengzi |
| 6  | Heshun   | 22 | Tianning| 38 | Pingyuan | 54 | Jiewu   |
| 7  | Tuantian | 23 | Pingda  | 39 | Nongzhang| 55 | Hua     |
| 8  | Gudong   | 24 | Mucheng | 40 | Zha     | 56 | Huguo  |
| 9  | Xinhu    | 25 | Hetou   | 41 | Xincheng | 57 | Jinghan |
| 10 | Mingguang| 26 | Bizhai  | 42 | Jiucheng | 58 | Qingping |
| 11 | Qushi    | 27 | Lameng  | 43 | Xima    | 59 | Wangzishu |
| 12 | Qingshui | 28 | Xiangda | 44 | Yousongling| 60 | Zhangfeng |
| 13 | Houqiao | 29 | Zhenan  | 45 | Zhanxi  | 61 | Saihao |
| 14 | Ruidian | 30 | Longshan| 46 | Sudan   | 62 | Longba |
| 15 | Jietou  | 31 | Longxin | 47 | Lianhuashan| 63 | |
| 16 | Tengyue | 32 | Longjiang| 48 | Mangyun |

Figure 3. The estimated VCAP values of the 62 towns in Yunnan, P.R. China, in 2005. The blue points represent the 62 towns in Yunnan. The red bars refer to the estimated VCAP values based on the temperature and rainfall in corresponding towns and time steps (i.e., 16 days for each time step).
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For each time step $t$, we have a vector of reported infections $y(t) = \langle y_1(t), \cdots, y_N(t) \rangle$, which represents the number of $P. vivax$ infections at each individual town. Based on the proposed spatial transmission model, we can estimate the number of infections $o(t+1) = \langle o_1(t+1), \cdots, o_N(t+1) \rangle$ at time step $t+1$ by treating $y(t)$ as an input. In other words, when an input pattern $y(t)$ is presented to the network, it produces an output $o(t+1)$, which is usually different from the number of reported cases $y(t+1)$ at time step $t+1$. Suppose that we totally have a $T$ number of time steps, that is to say, we have a training set \{$(y(1), y(2), \cdots, y(T), y(T+1))$\} consisting of $T$ ordered pairs of $N$ dimensional vectors (i.e., input-output patterns). In this case, the problem of inferring underlying transmission networks of $P. vivax$ is to learn the parameters $\beta, \gamma$, and link weights (i.e., $w_l$) of $G(V, L)$ by minimizing the sum of squares of error between the estimated numbers of infections (i.e., $o(t)$) and the observed numbers of infections (i.e., $y(t)$) for all towns and time steps, that is,

$$
\min E = \frac{1}{2} \sum_{t=1}^{T} \langle y(t+1) - o(t+1) \rangle^2.
$$

To solve the problem, we can use the backpropagation algorithm. The algorithm consists of three steps: (i) feed-forward computation, (ii) backpropagation computation, and (iii) weight updates.

**Step 1: Feed-forward computation.** Given an initial $W$ and the input vector $\tilde{y}(t)$, the estimated output $o^{(l)}(t)$ at layer $s_k$ can be calculated as follows:

![Diagram](Figure 4) A illustration of modeling infection risks of $P. vivax$ at each individual town. The notion of vectorial capacity ($\text{VCAP}$) is defined as “the number of potentially infective contacts an individual person makes, through vector population, per unit time.” The notion of entomological incubation rate ($\text{EIR}$) is defined as the number of infectious bites received per day by a human being. The calculation in this paper is based on the work of Ceccato et al. [6] and Smith and McKenzie [15].

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Then, the vector of weights $\beta_i$ represents the control impact of each node, $Z(t)$ is the number of imported cases, and the links between two hidden layers are determined by the transportation network structure.

Moreover, the algorithm will be stopped when there are successive 10 times that the change of $E$ is less than 1.

**Data collection and parameter settings**

The following data are involved in constructing our spatial transmission model and recurrent neural network model to infer the underlying transmission networks of $P.\,vivax$ among 62 towns in Yunnan, P.R. China.

- **Malaria cases.** We collect the cases of $P.\,vivax$ infection reported in 2005 from the China Information System for Disease Control and Prevention [20]. Although it is obligatory for any medical institutions and hospitals to report clinically confirmed infection cases into the system, it is ineluctable that some infection cases are under-reported [21]. While in this paper, we focus only on the $P.\,vivax$ infections that have been reported by the system. In other words, we do not consider the possible unreported cases of the $P.\,vivax$ infections. Specifically, we pay special attention to the geographical spread of $P.\,vivax$ among 62 towns in four adjacent counties in Yunnan, each of which has the annual incidence rate larger than 1/10,000 for at least one year. For each reported case, we collect the infection date and location from the system.

- **Temperature and rainfall.** We collect temperature and rainfall data of Yunnan in 2005 to estimate the transmission potential of $P.\,vivax$ for individual towns, which are located in the area between longitude ranging from 94.12134°E to 108.6718°E and latitude ranging from 20.62096°N to 29.37646°N. For the temperature, we use the Moderate Resolution Imaging Spectroradiometer (MODIS) to estimate near-surface air temperature, which are available on an 8 day basis at 1 km spatial resolution [22]. For the rainfall, we use the Tropical Rainfall Measuring Mission (TRMM) product to estimate...
daily precipitation, which are available on a 0.25 degree spatial resolution (about 26 km spatial resolution) [23]. Since the available MODIS and TRMM data have different spatial resolutions, we first project the TRMM data into the same resolution with MODIS data (i.e., 1 km spatial resolution). In doing so, many spatial grids may have the same values of daily precipitation. Such a deficiency can be addressed if more accurate estimates are available in the future. Then, we aggregate the daily precipitations on an 8 day basis to match the temporal resolution of the MODIS data. Finally, by respectively averaging the aggregated MODIS and TRMM data in a time duration $\Delta t = 16$, we can calculate the value of $FCAP$ for each individual town based on the model proposed by Ceccato et al. [6].

- **Population size.** The population size of each town is based on the national census in P.R. China. In the past decade, China conducted two national censuses, i.e., the fifth national census in 2000 and the sixth national census in 2010. However, since some administrative divisions and towns in Yunnan had been restructured after 2005, the sixth national census cannot reflect the population sizes of such towns obtained from the China Information System for Disease Control and Prevention in 2005. In this paper, we set the population size of each town based on the fifth national census in 2000 [24].

- **Time period studied.** It can be observed from surveillance data that the malaria transmission in Yunnan exhibits a seasonal pattern. In this paper, we focus mainly on the high-transmission months from April to October in 2005.

- **Duration of the time step.** Although P. vivax parasites may stay dormant for a long period after the primary infection is cleared from the bloodstream [25], the incubation period of P. vivax is usually from 12 to 20 days. In this paper, we set $\Delta t = 16$ to aggregate the time series of reported cases into different time steps. There are totally 12 time steps.

- **Road transportation network.** The road transportation network among the 62 towns is identified by using Google Maps API. If there is a direct road between two towns without passing through other towns, the road between the two towns will be included. Figure 6 illustrates the identified road transportation network, where the diameter is equal to 9. In other words, we have $s_d = 9$.

The proposed models have presented a general way to investigate the geographical spread of P. vivax based on surveillance data, which involve both the heterogeneous transmission potential of P. vivax and a machine learning algorithm. Based on the available one-year surveillance data, the demonstrated models are able to arrive at some informative results. Accordingly, if more malaria cases are collected from surveillance data across multiple years, the accuracy of our models will be further improved.

**Results**

The number of reported P. vivax cases for each individual town shows a certain degree of spatial heterogeneity. Figure 7 demonstrates a smoothed surface map with respect to the number of reported cases in individual towns in Yunnan, P.R. China. The map is generated using ArcGIS version 10.0 (ESRI; Redlands, CA, USA), where the kernel density estimator with search radius 0.2 is employed. The size of a node in blue corresponds to the total number of reported cases in 2005, while the colored surface represents the hotspot density magnitude of the P. vivax cases after smoothing. Four obvious hotspots can be observed, that is, the areas in red around the towns of Wuhe, Gudong, Pingyuan, and Jinghan.

Based on the annual case reporting system in P.R. China over the last several years [11,12], we assume that the fraction of imported cases among all the reported P. vivax cases in the 62 towns is at least 60%. Accordingly, we can estimate the proportion of imported cases for each individual town, that is, the vector $\gamma$ for the 62 towns. Figure 8 shows the estimated proportion of imported cases for each individual town under four scenarios with different percentage of imported cases in the total number of reported cases (i.e., 60%, 70%, 80%, and 90%). The error bars demonstrate the standard deviations, which refer to the variation of the estimated results for the four scenarios. It can be observed that for most towns, the proportion of imported cases does not vary too much. This is reasonable because international labor/tour mobility may have certain regular temporal or spatial patterns [26]. Specifically, it can also be observed that the town Wuhe has the largest proportion of imported cases among the 62 towns. This is consistent with the situation that Wuhe is the hotspot of malaria transmission (see Figure 7). From the viewpoint of active surveillance and intervention, we can pay special attention to those towns with a larger proportion of imported cases, namely, Wuhe, Tuantian, Mingguang, Tengyue, and Longjiang.

Figure 9 illustrates the values of weight matrices for the four scenarios with different percentages of imported cases. It seems that the inferred transmission networks of P. vivax (i.e., the weight matrices) show different patterns when the total percentage of imported cases changes. Particularly, it can be observed that as the total percentage of imported cases increases, the values of the diagonal entries vary dramatically. Note that the diagonal entries in a weighted matrix represent the severity of P. vivax transmission within individual towns (i.e., self-propagation of malaria) associated with their local transmission potential. This is because there is only little change about the proportion of imported cases for each individual town as shown in Figure 8. In this case, as the total percentage of imported cases increases, the total number of P. vivax cases caused by local infections will decrease. In other words, the P. vivax cases of individual towns will become geographically sparse. In this case, some towns with high malaria transmission risks may need to contribute more to the number of reported P. vivax cases in other towns to minimize the sum of squares for error, which makes them much easier to be identified.

Give the total percentage of imported cases in the 62 towns in Yunnan, we can further assess the roles of individual towns during the P. vivax transmission. Based on the estimated weight matrix for the scenario with 80% imported cases, the towns can be classified into two typical categories: the self-propagating towns and the diffusive towns (see Figure 10). A self-propagating town $i$ has a relatively larger $w_{ii}$, which means that fewer new infections in this town will transmit to other towns. While a diffusive town $j$ has a relatively smaller $w_{jj}$, which means that new infections in this town will be more likely to transmit to other towns. Figure 10 shows an example of classification with two specific thresholds, i.e., 0.5 and 0.8. The towns with the proportion of self-propagation larger than 0.8 (respectively, less than 0.5) are classified into the category of self-propagating towns (respectively, diffusive towns). The names of the corresponding towns can be found in Table 1. In reality, the thresholds can be defined by domain experts based on their work experiences.

**Discussion**

With respect to the vector-borne pathogen (i.e., malaria), existing studies have shown that human mobility from one location
to another, which exhibits various spatial and temporal scales, is a key behavioral factor for its geographical spread. This is because human mobility influences their exposure to infectious vectors (i.e., mosquitoes), and further the malaria transmission [8,27,28]. Extensive studies have been conducted attempting to quantify human mobility patterns so as to indirectly predict the underlying malaria transmission networks. Such human mobility patterns can be constructed from various available data, such as survey [29], census data [30], airline transportation [31], mobile phone [9,32,33], or even by certain computational methods, such as the gravity model or its extension [34]. However, most of them emphasize only the impacts of human mobility, which cannot reflect the complex properties of malaria transmission. To step forward to understand the underlying transmission networks of \textit{P. vivax}, in this paper, we have considered both the dynamics of \textit{P. vivax} transmission and the impact of human mobility.

Another research direction focuses on understanding the critical features of host-vector-parasite interactions by building explicit mathematical models, which assume homogeneous mixing of the population [13]. Starting from the Ross model [35], a variety of differential equation models with different levels of complexity have been proposed to investigate the roles of demographic, socio-economic, and environmental factors (e.g., age, immunization, and migration), which are helpful to predict the effects of interventions on the model parameters. Along this line, to assess the effects of human mobility on the persistence of malaria, many spatial transmission models have been proposed [28,36,37]. One common limitation of these conceptual models is that the population of both human beings and mosquitoes are assumed to be fixed. However, researchers have shown that environmental factors (e.g., temperature and rainfall) have a significant impact on mosquito population as well as their biological cycles [38,39]. In this paper, we have adopted the notion of vectorial capacity (\textit{VCAP}) to characterize the heterogeneous transmission potential of \textit{P. vivax} at different locations. Specifically, a vectorial capacity model proposed by Ceccato et al. [6] is used to monitor changing malaria transmission potential within a town by taking into consideration the impact of temperature and rainfall on the bionomics of mosquitoes and the parasite extrinsic incubation period in mosquitoes.

The last decade has witnessed a great upsurge in studying and revealing the unifying principles of real-world systems by modeling them as complex networks [40–42]. Since then, lots of efforts have been made to investigate disease transmission in populations by integrating epidemic modeling with complex networks analysis (e.g., human contact heterogeneity [43]). Each node in a network can represent either an individual or a group of individuals to model disease transmission at the individual/metapopulation level [44]. Accordingly, the transmission dynamics on the network can be formulated by stochastic models on regular networks [45] or irregular networks [46]. The mean-field versions of stochastic models on regular networks correspond to the deterministic models for which the homogeneous mixing of the population is a good approximation. One major concern of these studies is to investigate the impacts of realistic network topologies (e.g., random networks [47], small-world networks [47,48], and scale-free networks [49]) on

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{network.png}
\caption{An illustration of the road transportation network among the 62 towns in Yunnan, P.R. China. The roads are obtained using Google Maps API. A direct road between two towns without passing through other towns will be included. doi:10.1371/journal.pntd.0002682.g006}
\end{figure}
the process and results of disease transmission. Different from these studies, in this paper, we have focused on inferring the underlying \textit{P. vivax} transmission based on a small-scale actual network (i.e., the road transportation network among the 62 towns in Yunnan). In the future, the proposed model may be considered for larger networks, in which a complex networks approach will be suitable.

Regarding the machine learning procedure, Liu et al. [50] have stated that the methods to infer underlying networks of disease transmission from observed incidences could be significantly different from those to infer the structures of diffusion networks from information flows due to the unique nature of disease transmission dynamics [51,52]. Existing methods consider merely temporal information to infer diffusion networks, and most of them are based on the assumption of independent cascading of information. On the contrary, malaria may spatially propagate due to human mobility in two ways: (i) infected persons may bring the pathogen from one location to another, and (ii) susceptible persons can become infected while traveling to high-transmission locations. Therefore, geographical malaria transmission is not independent cascading. Reasonable transmission networks can be discovered only when appropriate transmission models are formulated.

As for the predictability, it is always expected that there is a powerful model that can provide accurate predictions on the malaria transmission patterns. However, it is extremely challenging due to the complicated dynamics of malaria transmission. Based on surveillance data for scenarios with various percentages of imported cases among all reported \textit{P. vivax} cases, the hybrid model (i.e., the spatial transmission model and the recurrent neural network model) presented in this paper can help infer (i) the proportion of imported cases for individual towns, and (ii) the transmission networks of \textit{P. vivax} among the 62 towns. The results have shown that the proportion of imported cases for individual nodes (i.e., the value of vector $c$) is relatively stable for different percentages of imported cases (Figure 8), while the underlying transmission networks depend heavily on the total number of imported cases (Figure 9). In P.R. China, the number of imported \textit{P. falciparum} cases at the county level is released every year through an annual case reporting system. To further implement our models, it would be necessary to continuously monitor the imported \textit{P. vivax} cases. By doing so, our models may provide public authorities with new insights into active surveillance and control of \textit{P. vivax} transmission. Specifically, this can be achieved.

Figure 7. A smoothed surface map with respect to the total number of \textit{P. vivax} cases in each individual town. The size of the nodes in blue represents the total number of reported cases. The colored surface represents the hotspot density magnitude of \textit{P. vivax} cases after smoothing. doi:10.1371/journal.pntd.0002682.g007
by (i) identifying whether or not a particular \textit{P. vivax} case is imported during data collection in the front line, and (ii) analyzing the tempo-spatial patterns of imported \textit{P. vivax} cases across multiple years.

Last but not the least, this work is novel in that it provides a way to investigate the underlying malaria transmission patterns from the real-world malaria surveillance data [53,54]. Figure 11 illustrates a machine learning framework, which consists of the interactions between malaria transmission models and machine learning models. The framework consists of three interactive components:

- \textit{Malaria transmission models}. Based on the real-world problems that need to be investigated, appropriate transmission models

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**Figure 8. The estimated proportion of imported cases for each individual town in different scenarios.** The error bars represent the standard deviations of the four scenarios with 60%, 70%, 80%, and 90% imported cases in the total number of reported cases. It can be observed that for most towns, the proportion of imported cases does not vary too much.

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**Figure 9. The inferred \textit{P. vivax} transmission networks for scenarios with 60%, 70%, 80%, and 90% imported cases.** The colors represent the relative strength of malaria transmission from one town to another. Note that the diagonal entries refer to the self-propagation of \textit{P. vivax} within individual towns.

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can be developed ranging from conceptual homogeneous mixing models [13] to realistic data-driven agent-based models [44,55]. Once a model is developed, some parameters should be continuously obtained from surveillance system, such as the temperature and rainfall in this work. Meanwhile, some parameters would be difficult to obtain directly from surveillance systems, which may also determine the performance of the model.

- **Machine learning models.** For the parameters that cannot be directly obtained from surveillance system, we can infer them using appropriate machine learning methods [56]. The learning process should comprehensively concern the differences between the outputs of the transmission model and the observations from surveillance systems.

- **Surveillance systems.** The functions of surveillance systems in this framework are twofold: First, the surveillance data can serve as continuous inputs for a malaria transmission model, which is used to predict malaria transmission patterns. Second, the surveillance data can also perform as measures of an appropriate machine learning model such that both the malaria transmission model and the parameters in the model can be adjusted accordingly.

The integration of the spatial transmission model and the recurrent neural network model in this paper provides a typical implementation of this framework.

Finally, due to the data availability at the moment, the proposed models still have several limitations that are worthy of being improved and investigated in the future:

- **Biological parameters.** Most of the biological parameters have been set based on the study of Ceccato et al. [6] (see Table 2). To achieve more precise prediction, specific investigation in Yunnan should be conducted. For example, the gonotrophic cycle length of mosquitoes in Yunnan may differ from that in Africa.

- **Spatial heterogeneity.** The TRMM data for daily precipitation is about 26 km spatial resolution in this paper, which is not good enough to represent the heterogeneity of daily precipitation of individual towns. Moreover, more geographical factors may be involved to reflect the spatial heterogeneity, such as elevations and vegetation of individual towns.

- **Human mobility.** This paper has only considered the mobility of infected populations among the 62 towns. By quantitatively characterizing human mobility patterns (e.g., through calling records of mobile phones [9,32]), the results might be significantly improved. Further, for those countries/regions where human mobility from one location to another may further introduce new infections, more complex spatial transmission models should be involved into the framework [28,36,37].

- **Learning methods.** A recurrent neural network model is used to infer the underlying $P. vivax$ transmission networks, where a time step with a duration of 16 days is utilized. In the future, novel machine learning methods will be proposed to avoid such manual settings. Moreover, to improve the accuracy of the learning results, it is necessary and desirable to continuously collect the reported cases of $P. vivax$ infections every year.

- **Under-reported cases.** The performance of the proposed models in this paper depends on the quality of surveillance data (i.e., the reported cases of the $P. vivax$ infections). However, in reality, the infections may be under-reported [21]. To take into account the possible under-reported infections, more deliberated models should be incorporated into the machine learning framework.

- **Imported cases.** In this paper, the proportion of the imported cases in each individual town is assumed to be constant throughout the year. In the future, it would be desirable to investigate whether this value is dynamically changing over time.

- **Dynamic transmission networks.** Similar to the imported cases, the $P. vivax$ transmission among the 62 towns may also exhibit certain spatio-temporal patterns. To investigate the dynamic $P. vivax$ transmission networks, it would be helpful to refine our framework by involving stochastic transmission models.
Author Contributions
Conceived and designed the experiments: BS JL XNZ. Performed the experiments: BS. Analyzed the data: BS JL XNZ GJY. Contributed reagents/materials/analysis tools: BS JL GJY. Wrote the paper: BS JL XNZ.

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