Theory of a superluminous vacuum quanta as the fabric of Space

Abstract

Our observations of magneton with Ferrolens shows evidence pointing to such magneton entity, and more evidently in recent results with the synthetic vacuum unipole experiments. Physics formalism ansatz novel model analyses demonstrate how vacuum quanta may have sufficient energy for vacuum genesis, by constructing eigen spinors of zero point microblackhole Hamiltonian quantum mechanics with Helmholtz decomposition matrix of gradient and rotational tensors, that are characteristic of translational vortex fields. With these mathematical physics processes, we obtain resulting energy fields spatial property partial differential equations characterizing eigen state energetics of zero point vacuum quagmire, as well as eigen state vortex fields of micro black hole, both together making up plasmodial zones within quagmire. Specific eigen spinors Hamiltonian partial differential equations quantifying energy and fields eigen functions. Vacuum that is dipole vacuum may have superposition of complex input of quagmire vortex fields acting to create non–hermitian quantum relativistic physics.

Keywords: quantum cosmology, vacuum space quanta, Hamiltonian operator, eigen functions, magneton, observables, general formalism, Hamiltonian analysis, vortex vacuum eigen spinors, gradient zero point source rotational micro black hole sink tensors

Introduction

Energetics of a vacuum space quanta that maybe unit of fabric of vacuum space had been quite perplexing physicists over many centuries, from classical to relativistic to quantum mechanics.\(^1,2\) Classical physics with Galilean Newtonian equations of motion and Maxwell’s electric vacuum equations had started to analyze quantitatively nature of gravity, space, and time, although it was elusive to explain wholesomely universal phenomena from micro to macro universe.\(^3,4\) Einstein’s relativistic theories proposed a way of bringing together the concept of space and time, topologically, to explain gravity to unify all forces of nature known to humans: electromagnetism, strong and the weak nuclear forces, and the gravity.\(^5–11\) Fundamentally, pure, and applied mathematics had been all the while playing a major role in quantifying physics through enabling parametric measurements of observations.\(^12\) To explain the microcosm of universe, quantum mechanics with Schrodinger’s wave function Hamiltonian equations came to explain the duality of the wave and particle aspects, with de Broglie’s assertion of simultaneity of energy and matter presence.\(^13\) Standard Model had put together spectra of quantum particles, with Higgs Boson identifying observable as the mass giver for particles, that will evolve onto real matter into existence.\(^14\) Quantum density matrix had formed the flavor of special unitary symmetries constituting typical gage invariance,\(^15\) with many grand unified theories establishing necessity of monopoles existing to account for energy densities of universal systems. However, the question of origin of energy and of quantum vacuum had been eluding physicists’ total quantify ability. Parametric analysis with experimental observations had posed a measurement problem. In his original introduction of mathematically provable quantization of monopole – charge aspects, noting knowhow physics, Dirac argued quantitatively vacuum quantum necessitating existence of monopoles based on fundamentals of quantum mechanics.\(^16\) To understand about vacuum space quantum vortex systems, generalized and/or modified Maxwell equations to include monopoles had been advanced mathematically analytically.\(^17\) A detailed knowledge with mechanics of quantifying vortex systems to monopoles\(^18\) to more specific Lagrangian and Hamiltonian derivation mathematically of vortex systems suitable to analyze vacuum quagmire with monopole & the dipole had already been modeled.\(^19–23\) These studies show that monopoles’ physics had mechanics like the fluid system’s hydro dynamical vortex systems Searches for monopoles, with scientists all over the world, consisted of two categories experimentally typically: (1) detecting preexisting monopoles, (2) creating and detecting then new monopoles.\(^24–35\) Mathematical techniques explored here to solve eigen value problem might set a precedence to abstract who list observational physics with mathematical preciseness, applicable further to provable generalized quantum relativistic grand formalism. In this paper, Helmholtz decomposition fields are only considered to come up with general formalism, especially since research experimentation measurements with Ferrolens observational results have shown that magnetism is exclusively a dipole phenomenon, which in contrast to eclecticism, hence cannot be mono pole. If an isolated natural occurring magnetic monopole charge is found, it would not create a gauge field – force field spatially around it radiated in space, all energy flows inward with none radiated outside, whereas a monopole electric charge which is a physically spinning magnetic dipole charge, radiates energy to the outside and therefore can create a field.\(^34,35\)

Standard techniques established by vast amount of quantum physics literature on constructing, analyzing, interpreting, quantifying as well as problem solving eigenvalues, eigenmatrices, eigenvectors, and fields of Hermitian and/or non –Hermitian Hamiltonian operator\(^36–41\) generating characteristic energy and field spectrum were widely utilized here to configure quantum characterization of matrix systems. Within all theoretical endeavors, matrix rules and quantifiable formulations follow integrated procedures configured from the research of physics literature articles, samples of which appear in the reference list, with\(^44–46\) in this paper. Zero –point analysis of quantum vacuum would refer to energy at the vacuum quanta zero –point fluctuation energy.\(^46,48\) Micro –black holes considered here in analysis would essentially be quantum blackholes.\(^51,52\) General
theoretical modeling is extendable to ansatz modeling superluminal multiphase systems that will grand unify fields, while explaining how such high energies originate in primordial universe.

**Explanations of magneton, quantum magnet, and type of fields they exhibit**

The term magneton refers to the elementary magnetic dipole quanta of any magnetic dipole charge either if it is an electron or quark or any particle that has a 1/2 spin, i.e., fermions. The difference of the Bohr magneton with the term we are using “magnetons” is that the Bohr magneton refers to the bound electrons of an atom whereas the term magneton refers in general to the “Quantum Magnet” and magnetic moment of any particle either it is free or bound in the atomic structure. In any event, the magneton is a monopole charge. With that said, our observations with the ferrolens of the Quantum Magnet field reveals that it consists of two opposite magnetic monopole charges thus two joint counter rotating magnetic flux monopole vortices jointed together to form a magnetic dipole or else a magnetic flux dipole vortex. This is now exactly to what our term “magnetons” refers to, according to our research. However, any vortex field is essentially a monopole field, therefore our observation and previous research reveals that the nature of the Quantum Magnet is essentially Gilbertian in nature and not Amperian. Thus, it effectively consists of two joint monopoles of opposite magnetic charges, the only form in our space time magnetic monopole charges can exist, i.e., jointly in a dipole formation.

Now, one of the central emphases with theory of the paper will be based on the conjecture that in our space–time these dipole magnetons can exist only as dipoles but in the super luminous energy phase of vacuum space, per Figure 1, the magnetons exist only as monopole energy vortices thus monopole magnetons, vibrating at super luminous speed and are like the pixels and elementary quanta of discrete vacuum space occupying each point of it. Consequently, in the fabric of our space time, for whatever reason these monopole magnetons lose their super luminous kinetic energy and drop down their energy level to luminous or sub luminous, brought out in Figure 1, they change phase and fall into our space time and instantly join into elementary magnetic dipoles, thereby forming the basis of fermionic matter in our universe. In the super luminous phase of vacuum space, this is totally undetectable by us and perceived by us as “empty space” in our space time.

**Figure 1** Schematic showing super luminous phase of vacuum space monopole magnetons essentially empty space manifesting subsequent phase transitions. Schematic sketching of phase transitioned luminous and sub luminous phase of vacuum space Einsteinian space time formation of dipole magnetons the basis of all fermionic matter in our Universe

**Experimental interpretations**

Our recent observations of magneton with Ferrolens quoted literature briefly show within the Figures 2 & 3 real–time observations of quantum field magnetism (QFM) of vortex dipoles, as well as physical mechanism explaining classical macroscopic electric E-field of a macro vacuum quantum dipole field, having vortex casualty effects, that are observed with the Ferrolens. Hedgehog field lines displayed by the Ferrolens, diverging out of the unipolar vacuum ring array’s vortex field shows effect of synthetic monopole quasi particle effect, like a ferro vacuum Dirac quantum vacuum monopole trap, referring to Figure XI (source: Emmanouil Markoulakis et al.). Also, screw –like unipole vortex formations, and non–classical vortex quanta, that appear as Quantum Magnet Field (QMF) Figure IV & X (source: Emmanouil Markoulakis et al.) are indicative of special features of monopole –like unipole synthetic vacuum array. Apart from our recent results, highlighted above suggesting monopoles spontaneously transform to dipoles, further observation with the vacuum 3D fields visualizations have proved that magnetons form the fundamental fields and that they are constituted by uni poles, quite likely building blocks of everything universally.

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Figure 2 (a) A logarithmic spiral. (b) QFM vortex dipole field magnetism. (c) left arm of spirural segment of the QFM. (d) Right arm spiral segment, these measurements comparatively show real-time observations originally per Figure VI (source: Emmanouil Markoulakis et al.) measurements with the Ferrolens.

Figure 3 Physical mechanism for explaining classical macroscopic E-field of macro vacuum quantum field dipole magnetism with vortex casualty effect originally Figure VI (source: Emmanouil Markoulakis et al.) observations with the Ferrolens.

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Theoretical results observables formalisms

We are attempting to establish theoretical basis to mathematically analyze these systems, with a key goal of identifying observables that are provable verifiably with experimental techniques, such as the quantum vacuum –optic flux viewer Ferrolens to probe inside the ferro vacuum materials, as well as Bose –Einstein condensate that can detect polar –core spin vortices especially of Dirac monopole. Standard techniques established by vast amount of quantum physics literature on constructing, analyzing, interpreting, quantifying as well as problem solving eigenvalues, eigen matrices, eigenvectors, and fields of Hermitian and/or non –Hermitian Hamiltonian operators26-45 generating characteristic energy and field spectrum are widely utilized to configure characterization of quantum vortex systems considered here. In all theoretical endeavors, matrix rules and quantifiable formulations follow integrated procedures that are adapted from the research of physics literature articles, samples of which appear in the reference list, with15-48,62,64-65 in this paper.

Simple reasons that justify formalism, applying Helmholtz decomposition fields analysis of vortex dynamics:

1. Magnetron33 experimental observations measurements show that the vortex fields are main characteristics. Helmholtz decomposition fields have already in –built rotational (vortex) fields and the gradient fields,27,62-69 which provide driving force to vortex fields, metrics, that can be expressed as a 2x2 matrix.

2. It is possible to transform from Helmholtz metrics, using Coulomb gage that will link to Coulomb branch gage with Hilbert series having SuperSymmetry (SUSY) Quantum Field Theory (QFT) charge conjugation.33,70 We can then link charge conjugation to rotating charges per Dirac Maxwell Einstein Kerr Newmann metrics.71,72

3. Hence, in this formalism, we adopt Helmholtz decomposition fields tensor matrix approach, due to above mentioned reasons.

Generalized formalism hamiltonian helmholtz eigenfields

Helmholtz mathematical physics theorem62 describes how a vector field can be expressed as a gradient scalar potential and a curl of vector field potential. We will expect the curl of the field being zero at the zero point,63 where authors have argued that for each stationary classical background field there is a ground state of the associated quantized field; this is the vacuum for that background. Helmholtz theorem has generality that can be used to connect quantum with relativistic physics.64 On the other hand, gradient field of zero at a black –hole with a nonzero curl65 causes highly energetic convection within increasing internal pressure asymptotically; here authors have brought out the effect of rotation on simulations of black hole events at the LHC showing that the angular momentum of the black hole cannot be ignored, and it makes a non –trivial contribution for most of the lifetime of the black hole. A key consequence of the rotation of the black hole is that the Hawking radiation is no longer isotropic, making it more difficult to infer space –time parameters from measurements of the emitted particles.65 In this letter, they had studied the angular distribution of the Hawking emission of non –zero spin particles with specific helicity on the brane, arguing that the shape of the distribution could be used as a measure of the angular momentum of the black hole.65

The Helmholtz theorem vector decomposition of field66 equates F = −∇Φ + ∇xA, where F is a vector field defined on a bounded domain V ⊆ ℝ3, which is twice continuously differentiable, having surface S enclosing domain V. F then thus can be decomposed into a curl –free component and a divergence –free component, such that any sufficiently smooth, rapidly decaying vector field in three dimensions can be resolved into the sum of an irrotational (curl –free) vector field and a solenoidal (divergence –free) vector field. This is known as the Helmholtz decomposition,36 with Φ = scalar potential; A = vector field potential; thereby, F = − grad Φ + curl A.

Upper and the lower indices, such as εμν and εμν , considered here in our detailed analysis of the general field tensors, follow normal tensor calculus mathematical notations.67 The zero –point vector field above brings out interesting situation of curl A → 0 , which is justifiable since rotational component will not exist at zero –point, although grad Φ ≠ 0 ; conversely, at a micro –black –hole, F → 0 , where the field may be collapsed electro vacuum light – electric + vacuum – vector field, and then ∇xF = ∇Φ – perhaps manifesting as Hawking radiation out of zero –point within a micro –black –hole. This is a conjecture borne out of Poincare’s Theorem stating that if ∇xF = 0 (i.e., F(x) is an irrotational field) in a simply connected neighborhood U(x) of a point x, then in this neighborhood, F is the gradient of a scalar field g(x).68 Rotational component is associated through Helmholtz decomposition to pressure, especially in fluid flow.69

Oliverknill70,71-73 highlights references related to detailed Helmholtz decomposition of the gradient and the rotational fields, considered extensively here to come up with general formalism Hamiltonian operator analysis quantum relativity. Also, mathematical matrix operational manipulations with outer and inner product space applied mathematical physics principles are listed also with63-64 containing Dirac matrix quantum notations. Authors have adapted many techniques applied to quantum physical analysis within the framework of the quantum field theory, as well as Hermitian and non –Hermitian Hamiltonian operator quantum relativistic physics with quaternions, encountered often in these systems. Already, the reasons for applying Helmholtz decomposition fields analysis of vortex dynamics have been mentioned above, consistent with physics literature.67,68-72 Mathematically, matrix quantum techniques with outer product of Helmholtz decomposition density field matrix are utilized to come up with eigenvector fields Hamiltonian characteristics68-71 below.

Outer product helmholtz decomposition density field matrix eigenvector operators constructs

$$|\hat{e}_{11}\hat{e}_{22}|e^{11} = \left(\hat{e}_{1,\mu\nu}\hat{e}_{2,\mu\nu}\right)\left(\hat{e}_{1,\mu\nu}\hat{e}_{2,\mu\nu}\right)$$

with $e_{\mu}$ : Helmholtz decomposition rotational field; $e_{\nu}$ : Helmholtz decomposition gradient field; $\mu$, $\nu$ are lower and the upper referential frame tensor calculus notations.67 $|\hat{e}_{11}\hat{e}_{22}e^{11}|$ gives the outer product of both of the fields with the indices to generate 2x2 Dirac matrix forms($\hat{e}_{1,\mu\nu}\hat{e}_{2,\mu\nu}$), which is equivalent to vector forms ($\hat{e}_{1,\mu\nu}$), ($\hat{e}_{2,\mu\nu}$). Note that tensor notations fields are true for rotational and the gradient fields, permuted to the index values to have representation of both senses with rotations as well as the gradients, thereby, upward, downward, outward, & the inward field tensors are fully generalized by this format. All the matrix manipulations to achieve quantum derivations have normal techniques employed conform to those given in physics literature,67,68 as also mentioned above.

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To get eigen values of characteristic field matrix above, we equate
\[ |A - \lambda I| = 0; \text{ hence} \]
\[ (\epsilon_{\mu\nu} - \lambda \epsilon_{\mu\nu}^{\mu\nu}) = 0 \]& solving quadratic equation in \( \lambda \):
\[ \lambda = (1/2) \left\{ (\epsilon_{\mu\nu} + \epsilon_{\mu\nu}) \pm \left[ (\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu} \right]^{1/2} \right\}. \]

Therefore,
\[ \lambda = (1/2) \left\{ (\epsilon_{\mu\nu} + \epsilon_{\mu\nu}) \pm \left[ (\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu} \right]^{1/2} \right\} \]
\[ \lambda_1 = (1/2) \left\{ (\epsilon_{\mu\nu} + \epsilon_{\mu\nu}) + \left[ (\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu} \right]^{1/2} \right\} \]
\[ \lambda_2 = (1/2) \left\{ (\epsilon_{\mu\nu} + \epsilon_{\mu\nu}) - \left[ (\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu} \right]^{1/2} \right\} \]

Thus, eigenmatrix eigenvector \(|\Psi_{1,1}\rangle\) with eigenvalue \( \lambda_1 \):

\[ \left( 0.5(\epsilon_{\mu\nu} - \epsilon_{\mu\nu}) - [(\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu}]^{1/2} \right) \epsilon_{\mu\nu} = 0 \]

Solving these equations and normalizing with respect to \( \Phi \) values

Two eigenvectors with eigenvalue \( \lambda_1 \) form general:

\[ \left( 0.5(\epsilon_{\mu\nu} - \epsilon_{\mu\nu}) - [(\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu}]^{1/2} \right) \epsilon_{\mu\nu} \]

Equations (6.1) and (6.2) together form Equation (6).

Similarly, other two eigenvectors with eigenvalue \( \lambda_2 \) form

\[ \left( 0.5(\epsilon_{\mu\nu} - \epsilon_{\mu\nu}) - [(\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu}]^{1/2} \right) \epsilon_{\mu\nu} \]

Equations (11.1) and (11.2) together form Equation (11).

Two eigenvectors with eigenvalue \( \lambda_2 \) = \((\epsilon_{\mu\nu}\epsilon_{\mu\nu})^{1/2}\)@zero - point:

\[ \left( -\epsilon_{\mu\nu}\epsilon_{\mu\nu} \right) \epsilon_{\mu\nu} \]

Equations (12.1) and (12.2) together form Equation (12).

Typical eigenvectors micro black hole vector fields

Only gradient with \( \epsilon_{\mu\nu} \) & \( \epsilon_{\mu\nu}^{\mu\nu} \) tensor fields are expected to be active. However, \( \epsilon_{\mu\nu} \) & \( \epsilon_{\mu\nu}^{\mu\nu} \), up and down curl of the tensor fields are expected to be zero. Therefore, equation (2) will become:

\[ \lambda_1 = (1/2) \left\{ (\epsilon_{\mu\nu} + \epsilon_{\mu\nu}) \pm \left[ (\epsilon_{\mu\nu} - \epsilon_{\mu\nu})^2 + 4\epsilon_{\mu\nu}\epsilon_{\mu\nu}^{\mu\nu} \right]^{1/2} \right\}. \]

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\[ \lambda = \left( \frac{1}{2} \right) \left( (\epsilon_{\nu \mu} + \epsilon_{\mu \nu}^*) + \left( (\epsilon_{\nu \mu} - \epsilon_{\mu \nu}^*)^2 + 4\epsilon_{\nu \mu \rho} \epsilon_{\mu \nu \rho}^* \right)^{1/2} \right) = \left( \frac{1}{2} \right) \left( (\epsilon_{\nu \mu} + \epsilon_{\mu \nu}^*) \pm (\epsilon_{\nu \mu} - \epsilon_{\mu \nu}^*) \right). \]

That is,

\[ \lambda_1 = \epsilon_{\nu \mu}, \]

\[ \lambda_2 = \epsilon_{\mu \nu}^*. \]  

(13)

(14)

Thus, eigenmatrix eigenvector \( |\Psi_{1 j}\rangle \) with eigenvalue \( \lambda_1 = \epsilon_{\nu \mu} \):  

\[
\begin{pmatrix}
0 \\
\epsilon_{\mu \nu}^* - \epsilon_{\nu \mu}^* \\
0
\end{pmatrix} \begin{pmatrix} \Psi_{1mb} \\ \Psi_{2mb} \end{pmatrix} = 0
\]

(15)

Eigenvector with eigenvalue \( \lambda_1 = \epsilon_{\nu \mu} \) @microblackhole:

\[
\begin{pmatrix}
1 \\
0
\end{pmatrix}
\]

(16)

Similarly, eigenmatrix eigenvector \( |\Psi_{1 j}\rangle \) with eigenvalue \( \lambda_2 = \epsilon_{\mu \nu}^* \):

\[
\begin{pmatrix}
\epsilon_{\nu \mu} - \epsilon_{\mu \nu}^* \\
0 \\
0
\end{pmatrix} \begin{pmatrix} \Psi_{1mb} \\ \Psi_{2mb} \end{pmatrix} = 0
\]

(17)

Eigenvectors with eigenvalue \( \lambda_2 = \epsilon_{\mu \nu}^* \) @microblackhole:

\[
\begin{pmatrix}
0 \\
1
\end{pmatrix}
\]

(18)

**Hamiltonian operator eigenfields zero point gradient & microblackhole rotational eigenspinors**

In zero point (zp) Hamiltonian, \( H_{zp} \), operating on wavefunction, \( |\Psi_{zp}\rangle \), generating zero –point energy, \( E_{zp} \), gives:

\[
H_{zp} |\psi_{zp}\rangle = E_{zp} |\psi_{zp}\rangle
\]

(19)

Procedures with physics literature as only sense –like fields are expected to occur in zero –point regions, with no time fields, only gradient Hamiltonian exists: \( H_{zp} = i\hbar V \).

(20)

Equation (11)(Equations (11.i) and (11.ii)) giving eigenvectors with \( \lambda_{zp} = (\epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*)^{1/2} \):

\[
|\lambda_{zp}\rangle = \left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{0.5}
\]

(21.i)

\[
\left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2} - \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \]  

(21.ii)

Equations (21.i) and (21.ii) together form Equation (21).

Equations (19), (20), & (21) will give result:

\[
H_{zp} |\lambda_{zp}\rangle = i\hbar \left( V_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{0.5}
\]

(22.i)

Equations (22.i) and (22.ii) together form Equation (22).

Performing differential algebraic manipulations, like Equation (19), having set of differential equations, for \( \lambda_{zp} = (\epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*)^{0.5} \)

per the Equation (21), will give following equations:

\[
\left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2} (\tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* - \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*) = E_{zp} \left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2}
\]

(23)

\[
\left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2} \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* = E_{zp} \epsilon_{\mu \nu}^*
\]

(24)

Per field –energy physics literature – listed here, we may write fields as systems 2nd order differentials of energy, appropriately taking care of indices within the procedures; therefore,

\[
\epsilon_{\mu \nu}^* = \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} (\tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* - \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*)
\]

(25)

Applying these equalities, and simplifying Equation (24), we can write:

\[
E_{zp} = \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* - \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2}
\]

(26)

Inputting \( E_{zp} \), per the Equation (26) into Equation (8), and simplifying after multiplication with \( (2i\hbar) \left( \epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2} \), we obtain resulting property with partial differential equation characterizing eigenstate energetics of zero point vacuum quagmire:

\[
\left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} = \left( (2i\hbar) \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \right)
\]

(27)

For \( |\lambda_{zp}\rangle = (\epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^* \right)^{1/2} \) per the Equation (21), similar calculations applying symmetry equivalents, we will obtain result:

\[
\left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} = \left( (2i\hbar) \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \right)
\]

(28)

Equivalently,

\[
\nabla^2 E_{\nu \mu} \nabla^2 E_{\mu \nu} = \left( (2i\hbar) \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \left( \tilde{\epsilon}_{\nu \mu}^* \mu_{\nu \mu} \tilde{\epsilon}_{\mu \nu}^* \right)^{1/2} \right)
\]

(29)

Similarly, \( \lambda_{zp} = -(\epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*)^{1/2} \) @zero –point will give resulting property with partial differential equations characterizing eigenstate energetics of zero point vacuum quagmire, by mathematically operating symmetry equivalents.

For \( |\lambda_{zp}\rangle = -(\epsilon_{\nu \mu} \mu_{\nu \mu} \epsilon_{\mu \nu}^*)^{1/2} \) per the Equation (12) and applying Hamiltonian procedure like \( |\lambda_{zp}\rangle \) above, we obtain equations:

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\[ \frac{\partial^2 E_{\mu\rho}}{\partial t^2} \left( \frac{\partial^2 E_{\mu\rho}}{\partial x^2} \right) = \left[ (2 - i\hbar) / i\hbar \right] \left( \frac{\partial^2 E_{\mu\rho}}{\partial x^2} \right) \left( \frac{\partial^2 E_{\rho\mu}}{\partial x^2} \right) \]

(30)

and for \( |\lambda_{mb}^*|^2 = |(E_{\mu\nu}^{\mu\nu} - E_{\rho\nu}^{\rho\nu})^2| \) per the Equation (12) and applying Hamiltonian procedure like \( |\lambda_{mb}^*|^2 > 0 \), we obtain equations:

\[ \left( \frac{\partial^2 E_{\mu\rho}}{\partial t^2} \right) \left( \frac{\partial^2 E_{\mu\rho}}{\partial x^2} \right) = \left[ (2 - i\hbar) / i\hbar \right] \left( \frac{\partial^2 E_{\mu\rho}}{\partial x^2} \right) \left( \frac{\partial^2 E_{\rho\mu}}{\partial x^2} \right) \]

(31)

Equivalently,

\[ \nabla^2 E_{\mu\rho}, \nabla^2 E_{\rho\mu} = \left( 2 - i\hbar / i\hbar \right) \nabla^2 E_{\rho\mu}, \nabla^2 E_{\mu\rho} \]

(32)

Symmetrical nature with energy indices, with \( \left( (2 - i\hbar) / i\hbar \right) \) having \( \approx \) value of order \( 10^{26} \) after numerically conjugating, then analytically interpreting will tell us that extremely high order energy transfers are possible at zero point, perhaps pointing to inflationary processes having quantum Diracian energy operational gradient exhibiting. One may note that if \( E_{\mu\nu}^{\mu\nu} \) & \( E_{\rho\nu}^{\rho\nu} \) are zero, it will imply that corresponding energy of \( 2^nd \) order derivative to be zero, pointing to the inflection of energy, that can induce consequent flow of flux due to gradient. This aspect we will notice that while analyzing micro black hole Hamiltonian values. Energy levels having order of magnitude of \( 10^{26} \) may not mean automatically that these are one chunk, but more likely \( n \cdot m^2 = 10^{26} \) metric units; if \( m \) is constituting positrons & electrons, then \( n \) may be as high as order of magnitude of \( 10^{35} \) particles, the flavor mass \( m \) of particles \( 10^{-20} \) to \( 10^{-31} \) mass units (nu) order of magnitude. These are likely progenitors’ propagators that may account for formation of plasma in star systems. These highest levels of possible inflationic Diracian energies will imply possibility of infinite energy, especially with superluminal multiphase systems, that will make sense of the finite mass constraints of the real universe; subsequently, we will be investigating these in greater detail further in our ongoing work. Mathematically, one may think of these as combinatorial particles within permutational density matrix of energy source of superluminal vacuum quagmire.

We will analyze now how the sink of the energies may be constituting crucial for creation of vast majority of Standard Model particles, within context typically micro –black holes. Hamiltonian operator eigen –fields rotational eigen spinors protocol will be examined further also.

In micro –black hole (mb) Hamiltonian, \( H_{mb} \) operating on wave function, \( \Psi_{mb} > \) generating energy, \( E_{mb} \), gives:

\[ H_{mb} \Psi_{mb} > = E_{mb} \Psi_{mb} > \]

(33)

\[ \left( \frac{\partial^2 E_{\mu\nu}}{\partial t^2} \right) \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) = \left[ (2 - i\hbar) / i\hbar \right] \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) \left( \frac{\partial^2 E_{\rho\nu}}{\partial x^2} \right) \]

(34)

Equation (12) will give eigenvectors with \( \lambda_{mb} = E_{\mu\nu} \):

\[ |\lambda_{mb}^*|^2 = (1) \]

(35)

Constructing time evolution field following physics procedures:

\[ E_{\mu\nu}(t) = E_{\mu\nu} \oplus e^{(-i\hbar / \hbar)} \]

(36)

Then on performing differentiation of \( E_{\mu\nu}(t) \) with respect to time, we will arrive at:

\[ \frac{\partial E_{\mu\nu}(t)}{\partial t} = E_{\mu\nu} \oplus (-i\hbar / \hbar) \]

(37)

On integration with respect to time, \( t = t_0 \) to \( t_f \), we get:

\[ \int \left[ \frac{\partial E_{\mu\nu}(t)}{\partial t} \right] dt = \int \left[ (-i\hbar / \hbar) \right] dt \]

(38)

After manipulations mathematically, we arrive at:

\[ H = \left( \hbar / (t_f - t_0) \right) \left[ \ln E_{\mu\nu}(t) \right] \]

(39)

Performing procedural relationship like in the Equation (25), we may write fields as systems of the \( 2^nd \) order differentials of energy, i.e. \( E_{\mu\nu} = \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) \), taking care of appropriate indices within the procedures as also, noting that the following relationships hold true:

\[ E_{\mu\nu, mb} = \int E_{\mu\nu} \cdot d\mathbf{r} \]

(40)

Operating Hamiltonian per the Equations (33), (35), & (39), we can get result:

\[ \left( \hbar / (t_f - t_0) \right) \left[ \ln \left| E_{\mu\nu} \right| \right] E_{\mu\nu} \left( \frac{1}{0} \right) = \int E_{\mu\nu} \cdot d\mathbf{r} E_{\mu\nu} \left( \frac{1}{0} \right) \]

(41)

Partial differential operations with respect to \( dr \) performing twice, the simplified result after having multiplication throughout by \( -i(t_f - t_0) / \left[ \hbar + \ln \left| E_{\mu\nu} \right| \right] \), we get this as the differential equation having \( 2^nd \) order terms, for \( \lambda_{mb} \) @ micro black hole:

\[ \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) = \left[ (2 - i\hbar) / i\hbar \right] \left( \frac{\partial^2 E_{\mu\nu}}{\partial x^2} \right) \left( \frac{\partial^2 E_{\rho\nu}}{\partial x^2} \right) \]

(42)

Equivalently,

\[ \nabla^2 E_{\mu\nu} - \left( i(t_f - t_0) / \hbar \right) E_{\mu\nu} \left( 1 + \ln |E_{\mu\nu}| \right) \nabla^2 E_{\mu\nu} + \left( i(t_f - t_0) / \hbar \right) E_{\mu\nu} \left( 1 + \ln |E_{\mu\nu}| \right) = 0 \]

(43)

Similarly, \( \lambda_{mb} = E_{\mu\nu} \oplus \) @ micro –black hole will give resulting property with partial differential equations characterizing eigen state rotational Hamiltonian characteristic operator time fields of micro –black hole vacuum quagmire; by mathematically operating symmetry equivalents eigen functions, Equation (18) will become:

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Partial differential operations with respect to $\partial t$, forming twice, the simplified result after having multiplication throughout by $-i(t_f - t_1)/[\hbar(1 + |\mu_{\nu \rho \sigma}|)]$, we get this as the differential equation having $2^{nd}$ order terms, for $\omega_{\nu \rho \sigma}:$

$$\left(\frac{\partial^2}{\partial \tau^2} \epsilon_{\alpha \beta} - \frac{i}{\hbar} \frac{\partial}{\partial \tau} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] \left[ \epsilon_{\alpha \beta} \right] \right) + \frac{i}{\hbar} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] = 0$$

Equivalently,

$$\nabla^2 \epsilon_{\alpha \beta} - \frac{i}{\hbar} \frac{\partial}{\partial \tau} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] \left[ \nabla \epsilon_{\alpha \beta} \right] + \frac{i}{\hbar} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] = 0$$

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$$\left(\frac{\partial^2}{\partial \tau^2} \epsilon_{\alpha \beta} - \frac{i}{\hbar} \frac{\partial}{\partial \tau} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] \left[ \epsilon_{\alpha \beta} \right] \right) + \frac{i}{\hbar} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] = 0$$

Equivalently,

$$\nabla^2 \epsilon_{\alpha \beta} - \frac{i}{\hbar} \frac{\partial}{\partial \tau} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] \left[ \nabla \epsilon_{\alpha \beta} \right] + \frac{i}{\hbar} \left[ \epsilon_{\alpha \beta} \left( 1 + \ln \epsilon_{\alpha \beta} \right) \right] = 0$$

**Theoretical results observable discussions**

We noted above, nature of general solutions giving eigen functions to be revealing vacuum fields energy possibly possessing higher order $10^{20}$ metric units at quantum zero point; these situations are analogous to situations that may be encountered at inflationary vacuum zero point, whose characteristic energies are well known in physics literature. Based on all these, we would be able to infer that Equation (46) would be capable of giving insight through micro –black hole general solutions’ eigen value eigen functions like “fields” equations. These are too analogous to the relativistic physics with macro black holes; hence these are further extensions to micro –black holes that have been actively considered subjects within physics literature. We can analytically quantitatively interpret with partial differential equations (43) & (46) these physics aspects. Especially evident while noticing, that time aspect $(t_f - t_1)$ can be quite analogous to real and proper time, with field up and down differentially spatially varying with relativistic systems. Also, notable are special requirements with rotational fields, $\epsilon_{\alpha \beta}$, both up and down indices stabilizing positive values due to logarithmic functionality, i.e. $\ln |\epsilon_{\alpha \beta}|$ and the apparent symmetry with $2^{nd}$ order, $1^{st}$ order, & $0^{th}$ order differential terms, per differential equations (32), (43), & (46).

**Summary**

Experiments, as well as measurements of real time observations of magneton by Ferrolens, reported earlier, was pointing to a fundamental vacuum quanta mechanism. The term magneton refers to elementary...
magnetic dipole quanta of fermions and having two joint counter rotating magnetic flux monopole vortices, forming magnetic dipole, and thus a quantum magnet. This is essentially Gilbertian having opposite magnetic charges. We propose space –time these exist only as dipoles within super luminous energy phase of “empty” vacuum space, which can phase transition to luminous or sub luminous space time, shown by schematics.

We applied Helmholtz decomposition fields with magneton experimental observations measurements showing the vortex field, reasoning that it is possible to convert from Helmholtz metrics onto Dirac –Einstein –Maxwell –Kerr –Newton metrics, by applying Coulomb gage. Ansatz generalized Hamiltonian quantum mechanics of vacuum quanta formalism was advanced here, constructing outer product Helmholtz decomposition field density matrix eigenvector operators’ Hamiltonian characteristics.

Helmholtz decomposition matrix consisted of both gradient up and down field tensors as well as the rotational up and down field tensors, that were reasoned to fit well mathematically to analyze zero –point and micro black hole in vacuum quanta. Eigen values as well as eigenvectors of characteristic general field matrix and specifically of zero –point and micro black hole eigen spinors’ vector fields were derived analytically quantitatively. Eigen matrix eigenvector $|\Psi_i, j > s$ with eigen value $\lambda s$ were quantified completely mathematically. These quantifications successfully eventually generated systems partial differential equations, characterizing zero –point and microblackhole vortex and gradient energy fields of vacuum quanta. Such quantification physics techniques are quite useful in knowing as well as analyzing super luminous fabric of space aspects of vacuum quanta. This formalism has already generality to model further magneto –electro vacuum quanta space, that we are verifying of vacuum quanta formalism was advanced here, constructing outer product Helmholtz decomposition field density matrix eigenvector operators’ Hamiltonian characteristics.

We hope having next set of papers on problem solving mathematical physics formalisms within well the framework of generalized Hamiltonian operator analysis, achieved here as a new ansatz, extending vacuum quanta analysis to superluminal multi phases systems modeling. This will be then capable of explaining paradoxical nature with physics, sorting quantitatively matter, antimatter, dark matter, dark energy, and the creation of stable geodesics within galactical star systems sustaining live cosmos.

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Conflicts of interest

Author declared there are no conflicts of interest.

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