Polaritonic Feshbach resonance

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A Feshbach resonance occurs when the energy of two interacting free particles comes into resonance with a molecular bound state. When approaching this resonance, marked changes in the interaction strength between the particles can arise. Feshbach resonances provide a powerful tool for controlling the interactions in ultracold atomic gases, which can be switched from repulsive to attractive\textsuperscript{3-4}, and have allowed a range of many-body quantum physics effects to be explored\textsuperscript{5,6}. Here we demonstrate a Feshbach resonance based on the polariton spinor interactions in a semiconductor microcavity. By tuning the energy of two polaritons with anti-parallel spins across the biexciton bound state energy, we show an enhancement of attractive interactions and a prompt change to repulsive interactions. A mean-field two-channel model quantitatively reproduces the experimental results. This observation paves the way for a new tool for tuning polariton interactions and to move forward into quantum correlated polariton physics.

A semiconductor microcavity is a unique system where exciton–polaritons emerge from the strong coupling between an exciton and a photon. The demonstration of Bose–Einstein condensation of exciton–polaritons in a semiconductor microcavity\textsuperscript{7} has attracted much attention and opened a wide field of research on polariton quantum fluids, such as superfluidity\textsuperscript{8}, quantum vortices\textsuperscript{9} and Bogoliubov dispersion\textsuperscript{10-12}. Many more examples could be proposed to highlight the fact that polaritons provide a concrete realization of a bosonic interacting many-body quantum system, complementing the work performed on ultracold atom systems.

Furthermore, polaritons exhibit a polarization degree of freedom, with a one-to-one connection to two counter circular polarizations for their photonic part. The different excitonic content of both polarization states results in asymmetric spinor interactions. Such spinor interactions offer a wide range of effects and a very rich physics to explore in semiconductor microcavities\textsuperscript{13-18}.

In this work, we demonstrate a Feshbach resonance in a polariton semiconductor microcavity. Polariton bieexcitonic resonant scattering is investigated through spectrally resolved circularly polarized pump–probe spectroscopy on a III–V based microcavity (Methods). To bring the energy of a two-lower polariton state into resonance with the biexciton state we change the cavity exciton detuning (Fig. 1a,c). We evidence the resonant polariton scattering by probing the anti-parallel spin polariton interactions when scanning the two-polariton energy across the bound biexciton state. We clearly show the enhancement of polariton interactions and the change of their character from attractive to repulsive. Moreover, we observe a decrease of the polariton resonance amplitude when the lower polariton energy is in the vicinity of the biexciton energy. The results are modelled by numerical simulations based on a mean-field two-channel model that includes coupling between polaritons and biexcitons as a key ingredient. It is worth mentioning that several works\textsuperscript{19-22} have already reported observations of coupling between polaritons and biexcitons without reaching the regime of the Feshbach resonance reported here.

The expected signatures of the Feshbach resonance phenomenon are twofold. First, a strong variation of the strength and sign of the scattering amplitude; second, a reduction of the free particle density through the coupling with the molecular bound state. Both are sensitive to the energy difference between the free particles and the molecular states. These two energy states refer, in our system, to the state of two anti-parallel spin lower polaritons and the biexciton state, respectively.

We investigate both experimental signatures of the Feshbach resonance. This coherent effect requires working in the coherent regime, therefore we set a zero delay between pump and probe (results from experiments with different pump–probe delays are presented in Supplementary Methods). For a given pump power, we measure through the transmitted probe beam the energy shift and the amplitude variation of the lower polariton resonance induced by the presence of the polariton population generated by the pump (Fig. 1b,d,e). From negative to positive cavity detuning, the energy of the two lower polaritons (2LP, one from the $\sigma_+$ polariton cloud created by the pump, and one $\sigma_-$ polariton coming from the probe) ranges from below to above the molecular biexciton state energy, passing through the resonance (Fig. 1c). In Fig. 2a, we plot the lower polariton energy shift versus exciton-cavity detuning for a polariton density of $5.1 \times 10^9$ polaritons cm$^{-2}$ generated by the pump. This result clearly shows a dispersive shape, characteristic of the resonant scattering. Indeed, in dilute atomic gas systems the Feshbach resonances are evidenced by a dispersive shape of the scattering length at resonance\textsuperscript{7}. In these atomic systems, the dispersive shape diverges in the case of magnetic Feshbach resonances with very long molecular lifetime\textsuperscript{22}. Here, however, a smooth dispersive shape shows up, similar to the case of optical Feshbach resonances with finite molecular lifetime\textsuperscript{23,4}. For polaritons, the finite lifetime of the molecular biexciton state prevents the dispersive shape form diverging at the resonance. Note that the sign and amplitude of the energy shift are related to the character and strength of the polariton interaction respectively. Our result directly shows that, at resonance, the energy shift switches from redshift to blueshift, demonstrating the drastic modification of the interaction character from attractive to repulsive. This measured shape provides clear evidence for a Feshbach resonance.

In Fig. 2b, we plot the variation of the polariton resonance amplitude as a function of the cavity detuning. This result shows the resonant conversion of two polaritons with anti-parallel spins into a biexciton. The simultaneous observations of the change of the polariton interaction character from attractive to repulsive together with the enhanced polariton loss through the coupling with the molecular biexciton state gives direct evidence for the polaritonic Feshbach resonant scattering. The resonance effect shown in Fig. 2a,b is located at an exciton-cavity detuning energy

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Figure 1 | Experimental scheme used for the polaritonic Feshbach resonance. a, The spin-down polariton energy varies as a function of the cavity detuning in the presence of a spin-up polariton population. In the perturbative regime, the lower polariton resonance shows a dispersive shape (orange line) around the crossing point with the bieexciton energy state (bold dashed line). At higher polariton spin-up densities, the lower polariton branch splits into two at the bieexciton crossing energy (solid white lines). This effect results from the strong coupling with the bieexciton (Bx) resonance. UP and LP branches stand for the upper and lower polariton resonances respectively. b, A pump beam creates a gas of spin-up polaritons (violet) and the probe introduces a few spin-down polaritons (orange), which interact with the gas. Inset b shows the transmission spectrum of the probe σ− without (black line) and with (red line) the presence of a spin-up polariton gas. c, Two-polariton energy with respect to the bieexciton state determines the interaction configuration: attractive (red arrows) or repulsive (blue arrows). The resulting polariton energy is depicted in Fig. 1a. d,e, Pump–probe spectra for polariton densities of 4.5 × 10^{10} cm^{-2} (d) and 1.5 × 10^{11} cm^{-2} (e), Cavity detuning is −1.1 meV. In e, the black arrow indicates the appearance of a new resonance resulting from the strong coupling between the LP branch and the bieexciton.

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Figure 1 | Polaritonic Feshbach resonance: experimental manifestations. a, Energy shifts of the pump–probe spectrum as a function of cavity detuning. b, \( \ln(P_{\text{ref}}/P_{\text{pump–probe}}) \) as a function of cavity detuning, where \( P_{\text{ref}} \) and \( P_{\text{pump–probe}} \) represent the amplitude of the lower polariton resonance without and with pump excitation, respectively. The blue circles are experimental results, orange and black lines show numerical simulations without and with polariton–biexciton coupling, respectively. The green region corresponds to the energy range where the two-polariton energy crosses the biexciton state energy, \( E_{\text{p+1}+E_{\text{p+1}}} \), and \( E_{\text{BX}} \) (Fig. 1c). Error bars represent ±3 standard deviations.

We then extract the energy shifts and the amplitude variations of the polariton resonance between the calculated \( n_p = 0 \) and \( n_p \neq 0 \) probe transmission spectra as a function of cavity detuning. In Fig. 2a,b, the orange lines represent, respectively, the polariton energy shift and amplitude variations obtained by the numerical calculations for \( n_p = n_0 \). Here, \( n_0 \) is a normalized polariton population density corresponding to the experimentally extracted polariton density of \( 5.1 \times 10^{10} \) polaritons cm\(^{-2}\). The other fitting parameters are summarized in the simulation section of Methods. Note that the calculated results overlap very well with the experimental plots, showing a very good agreement between theory and experiment. The plotted black lines correspond to the calculated energy shift and amplitude variations using the same parameters, but without the polariton–biexciton scattering term (\( g_{\text{BX}} = 0 \)). Here, only the background attractive anti-parallel spin polariton interaction exists. Note that even without the biexcitonic effect, the mean-field polariton energy shift and amplitude variations depend on the cavity detuning. In Fig. 2a (black curve), the polariton energy redshift increases according to the fourth power of the excitonic Hopfield coefficient\(^{22,25}\). The experimental results, however, strongly deviate from this behaviour when the biexciton resonance is approached. This result evidences the fact that the prominent enhancement of the energy redshift, as well as the change of sign of the interaction from attractive to repulsive, can only be accounted for by the polariton–biexciton coupling, confirming the polaritonic Feshbach resonance.

Concerning the change of amplitude of the polariton field, there exist two contributions. The first contribution is an effective positive increase of cavity detuning induced by the polariton energy redshift due to the background attractive interaction\(^{22}\), which reduces the photonic component of the polariton and therefore implies a decrease of the amplitude of the polariton resonance (black line in Fig. 2b). This contribution alone evidently does not reproduce the experimental results. The second contribution is the decay of two polaritons with anti-parallel spins into the biexciton channel as a
result of polariton–biexciton coupling. As is clearly shown in Fig. 2b (orange curve), to reproduce accurately the large decrease of the polariton resonance amplitude the polariton spin-up + polariton spin-down $\rightarrow$ biexciton scattering process should be introduced in the model.

We plot in Fig. 2c interaction and absorption ratios extracted from Fig. 2a,b respectively. Those ratios result from the total contribution (orange curves) divided by the background contribution (black curves). These two ratios evidence the usual behaviour of a scattering resonance. The absorption ratio (dashed curve) behaves as the expected scattering resonance profile due to the two-body loss process of lower polaritons when crossing the molecular state. The interaction ratio (solid curve) exhibits a dispersive shape of the scattering length, showing a large variation in terms of the sign and amplitude of the interaction strength crossing the biexciton resonance. Analogous observations are reported by Theis et al. in a $^{87}$Rb condensate in optical Feshbach resonance.

This model, in which we consider the interaction of the two anti-parallel spin polaritons with the molecular biexciton state, reproduces the experimental results very well. This is the resonant interaction term that governs a Feshbach resonance. In the present model, it is important to note that the coupling between polaritons and biexcitons, the coupling term $g_{\text{BX}}\sqrt{n_{\text{C}}}$, depends not only on the constant $g_{\text{BX}}$ but also on the excitonic content of polariton population $\sqrt{n_{\text{C}}}$. At low pump power, the pump polariton density is small and, consequently, this coupling term is weak. In this perturbative regime, the comparison between simulations and experiments shows excellent qualitative and quantitative agreement, demonstrating unambiguously the polaritonic Feshbach resonance.

We now turn to the investigation of the polaritonic Feshbach resonance in a system with a larger polariton population. We perform pump and probe measurements as a function of the cavity detuning using higher pump intensities to increase the polariton population. As the pump power is increased, a new resonance shows up at higher energy than the polariton resonance (Fig. 1e). In Fig. 3 we plot, for a polariton density of $1.6 \times 10^{11}$ polaritons cm$^{-2}$ generated by the pump, the energy shift of both polariton resonances and the amplitude variation of the lower energy polariton resonance as a function of the cavity detuning.

When the cavity detuning brings the two-polariton state energy close to the biexciton bound state energy then both resonances show an anti-crossing behaviour (Fig. 3a). The associated energy shifts obtained from the numerical simulations using the same parameters as for the lower power regime, but now with $n_p = 2.44 n_0$, are shown as full and dashed orange lines for the lower and higher energy resonances, respectively. The numerical results show remarkable quantitative agreement with the experimental results. We also show the numerical result obtained without considering the polariton–biexciton coupling ($g_{\text{BX}} = 0$) as solid black line, which clearly deviates from the experimental data. In this high-density regime, the appearance of a new resonance and the anti-crossing behaviour evidence the strong polariton–biexciton coupling. It is important to note that, to reach this strong coupling regime, the polariton–biexciton coupling energy $g_{\text{BX}}\sqrt{n_{\text{C}}}$ should be comparable to the linewidths of the involved states. In our system, the polariton–biexciton coupling strength is directly controlled by the density of polaritons through the pump intensity. Then, for the pump intensity used in Fig. 3, the polariton–biexciton coupling energy is of the same order as the biexciton linewidth. Indeed, in this regime, the polaritonic Feshbach resonance shows an anticrossing between these two states in addition to the change of the polariton interaction.

Moreover, as the spin-up polariton population is increased, the two spin-up spin-down polariton correlation is enhanced, which favours the biexciton creation. In Fig. 3b, we plot the amplitudes variations of the lower energy resonance shown in Fig. 3a. Enhancement of the amplitude variation with pump intensity and consequent increased losses with pump polariton population are evidenced. This supports the enhancement of the biexciton formation for the larger polariton population. The very good agreement between experimental and theoretical values corroborates our interpretation as a polaritonic Feshbach resonance.

All these results together demonstrate two different regimes of polaritonic Feshbach resonance. First, in the low-density regime, where polaritons and biexcitons show small interactions, the polariton–biexciton coupling energy cannot overcome the damping rate of the biexcitons $2\gamma_{\text{BX}}\sqrt{n_{\text{C}}} < \gamma_0$. Therefore, in this weak interaction regime, the manifestation of the Feshbach resonance exhibits a dispersive shape. In contrast, in the strong interaction regime $2\gamma_{\text{BX}}\sqrt{n_{\text{C}}} \sim \gamma_0$, polaritons and biexcitons states manifest an anticrossing. The splitting energy, proportional to twice the polariton–biexciton coupling term, increases for much higher pump intensities (not shown). As a result, the polariton population governs the polariton–biexciton coupling strength, which allows for the polaritonic Feshbach resonance to be tuned from the weakly to strongly interacting regime.

**Methods**

Our study is performed on a high-quality III–V microcavity. A single 8 nm In$_{0.5}$Ga$_{0.5}$As quantum well is sandwiched between a pair of GaAs/AlAs distributed Bragg-reflectors (DBRs). The exciton energy of the quantum well is 1.4866 eV and the Rabi splitting at zero detuning between the cavity and exciton energy is 3.26 meV (ref. 27). The measurements are performed at a temperature of approximately 4 K. We employ a counter-circular polarization configuration to investigate the polariton–polariton interaction with anti-parallel spins. To demonstrate the Feshbach resonance on the spinor polariton scattering, we carry out polarization-resolved pump–probe spectroscopy in transmission. We employ a heterodyne measurement technique$^{3,28}$, which markedly increases the signal to noise ratio. It allows one to resolve small probe beam energy shifts and to use a degenerate beam configuration. Figure 1bc shows the schematics of our pump–probe experiment. The sample is resonantly excited at $k = 0$ with a $\sigma^-$ circularly polarized pump pulse to generate a spin-up polariton population and probed at $k = 0$ using a counter-circularly polarized probe pulse. Because the cavity spacer layer is wedged, we tune the resonance energy of the cavity by moving the laser spot over the sample. The biexciton binding energy $E_{\text{BX}}$ is of the same order as the Rabi splitting. It is then straightforward to bring the energy of a two-lower-polariton state in resonance with the biexciton state by changing the cavity-exciton detuning (Fig. 1a,c). We repeat the experiment for different cavity detunings and different pump powers.

The laser source is a 125 fs pulse with a repetition rate of 80 MHz, which is separated into three pulses: pump, probe and reference. The pump spot size (2,200 $\mu$m$^2$) is larger than probe size (250 $\mu$m$^2$) to ensure the study of a uniform pump polariton density. We fixed the probe intensity at approximately one third the pump intensity in the low-density regime (Fig. 2). Then, increasing the pump intensity, the pump/probe density ratio is even larger. The centre frequency of the laser is set between the lower and upper polaritons. In our measurement we varied the LP energy only within 2 meV. As the laser spectrum is about 14.6 meV wide, the laser intensity is considered to be constant for all laser detunings. Both probe and reference beams are detected by a spectrometer and the spectrum of the probe pulse is numerically reconstructed.

**Simulation.**

The biexciton energy is determined as $E_X = E_X^0 - E_{{\text{BX}}} / 2$, with $E_{{\text{BX}}}$ being the biexciton binding energy. For the numerical calculation of Figs 2 and 3 we use the following parameters: the biexciton binding energy $E_{{\text{BX}}} = (1.5$ meV, a biexciton linewidth $\gamma_{\text{BX}} = 1.1$ meV. For the polariton–biexciton coupling, the exciton–exciton scattering term is set to $g_{\text{XX}} = 0.36$ meV/$\sqrt{n_{\text{C}}}$. The background interaction is $U_{\text{BG}} = -0.18$ meV$/n_0$, where $n_0$ is the normalized density of spin-up polaritons. The other parameters are the photon linewidth $\gamma_{\text{P}} = 0.3$ meV, exciton linewidth $\gamma_{\text{P}} = 0.6$ meV and Rabi coupling $\Omega_{\text{R}} = 1.63$ meV. Note that the same parameter values are used for all experiments, except for the polariton density $n_p$, which is adjusted when the pump density is changed. The excitonic density $n_x$ is expressed as a function of the polariton density $n_p$ through the expression:

\[
   n_x = \frac{2}{\sqrt{\sqrt{3} + 4\Omega_0^2}} \left( 1 + \frac{\delta}{\sqrt{\sqrt{3} + 4\Omega_0^2}} \right) \tag{1}
\]

where $\delta$ is the exciton–cavity detuning. Polariton density is estimated through the density of the excitonic component. In the higher-density experiment, we observe
a strong to weak coupling transition at the cavity detuning 0.87 meV. This means that, at this cavity detuning, the excitonic component of polaritons reaches the exciton saturation density $n_{sat}$, which is given by $n_{sat} = 7/16 \times 10^{11} \text{cm}^{-2}$ (ref. 29) for a Bohr radius of 12 nm in a single InGaAs quantum well. The polariton density can then be estimated using (1). To facilitate the extraction of the new upper resonance energy position in the large polariton population experiment (orange dashed line Fig. 3), we force $\gamma_L = 0$ in the model to enhance the peak transmission. Note that this procedure does not affect the resonance energy positions.

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Author contributions
N.T. and S.T. contributed to the experiment. N.T. performed the measurements and the authors contributed to numerous discussions and revised the manuscript.

Additional information
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Competing financial interests
The authors declare no competing financial interests.