A Deep Lyα Survey in ECDF-S and COSMOS. I. General Properties of Lyα Emitters at $z \sim 2$

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Abstract

Lyα emitters (LAEs) may represent an important galaxy population in the low-mass regime. We present our deep narrowband imaging surveys in the COSMOS and ECDF-S fields and study the properties of LAEs at $z = 2.23 \pm 0.03$. The narrowband surveys conducted at the Magellan II telescope allow us to obtain a sample of 452 LAEs, reaching a 5σ limiting magnitude of $\sim 26$ mag. Our Lyα luminosity functions extend to $L(\text{Ly}α) = 10^{41.8} \text{ erg s}^{-1}$ with a steep faint-end slope. Using multicolor ancillary data, especially the deep Spitzer/IRAC 3.6 and 4.5 μm photometric data, we obtained reliable stellar mass estimates for 130 IRAC-detected LAEs, spanning a range of $8 < \log(M_*/M_\odot) < 11.5$. For the remaining IRAC-undetected LAEs, the median-stacked spectral energy distribution yields a stellar mass of $\log(M_*/M_\odot) = 7.97^{+0.05}_{-0.07}$ and the rest-frame ultraviolet emission indicates a median star formation rate (SFR) of $\log(SFR/M_\odot\text{ yr}^{-1}) = -0.14 \pm 0.35$. There are six LAEs detected by the Spitzer/MIPS 24 μm or even Herschel far-infrared observations. Taking into account the six mid-IR/far-IR-detected LAEs, our LAEs cover a wide range in the SFR ($1 M_\odot\text{ yr}^{-1} < SFR < 2000 M_\odot\text{ yr}^{-1}$). Although LAEs as a population are diverse in their stellar properties, they are mostly low-mass star-forming galaxies and follow the star formation main-sequence relations or their extrapolations to the low-mass end, implying a normal star-forming nature of LAEs. The clustering analysis indicates that our LAEs reside in dark matter halos with $(\log(M_\text{h}/M_\odot)) = 10.8^{+0.56}_{-1.1}$, suggesting that they are progenitors of local LMC-like galaxies.

Key words: galaxies: evolution – galaxies: formation – galaxies: high-redshift – galaxies: luminosity function, mass function – galaxies: star formation

1. Introduction

The epoch at $z \sim 2$ is crucial in the history of galaxy evolution when the cosmic star formation rate (SFR) density reaches its peak (Madau & Dickinson 2014, and references therein). Detailed knowledge of massive (>10$^{10} M_\odot$) galaxies at this epoch has been widely investigated (e.g., Erb et al. 2006; Förster Schreiber et al. 2009; Steidel et al. 2014; Kriek et al. 2015; Burkert et al. 2016; Wuyts et al. 2016). On the other hand, low-mass galaxies at $z \sim 2$ pose a unique and important position in studying galaxy evolution because they are building blocks of local mature galaxies. However, our knowledge on low-mass galaxies (<10$^{10} M_\odot$) at $z \sim 2$ is still limited owing to challenges in identifying these faint galaxies. Large samples, on the other hand, are needed for a robust census of such galaxies. The narrowband imaging technique is an effective way of detecting Lyα emitters (LAEs) at specific redshifts (e.g., Malhotra & Rhoads 2002; Wang et al. 2005; Finkelstein et al. 2007, 2008; Gawiser et al. 2007; Gronwall et al. 2007; Nilsson et al. 2007; Pirzkal et al. 2007; Lai et al. 2008; Ono et al. 2010a, 2010b; Acquaviva et al. 2011; Zheng et al. 2016). Other methods such as integral-field spectroscopy (e.g., van Breukelen et al. 2005; Drake et al. 2017), slit spectroscopy (e.g., Rauch et al. 2008) and medium-band imaging (e.g., Steiavelli et al. 2001; Taniguchi et al. 2015; Sobral et al. 2018) have also been employed in finding LAEs. LAEs were found to be mostly composed of low-mass star-forming galaxies (e.g., Gawiser et al. 2006; Finkelstein et al. 2007; Pirzkal et al. 2007; Lai et al. 2008; Guaita et al. 2011; Nilsson et al. 2011; Shimakawa et al. 2017), although red massive star-forming LAEs do exist (e.g., Stiavelli et al. 2001; Finkelstein et al. 2008, 2009; Lai et al. 2008; Ono et al. 2010b; Acquaviva et al. 2011; Guaita et al. 2011; Nilsson et al. 2011; Oteo et al. 2012; Matthee et al. 2016). Therefore, LAEs can be used to probe the properties of low-mass galaxies at high redshifts.

In the past several years, a number of narrowband imaging surveys and spectroscopic observations have been carried out to search for LAEs at $z \sim 2$ (e.g., Nilsson et al. 2009; Guaita et al. 2010; Blanc et al. 2011; Cassata et al. 2011; Nakajima et al. 2012; Hathi et al. 2016; Matthee et al. 2016; Shimakawa et al. 2017). These surveys and deep multicolor ancillary data have made it possible to yield measurements of properties of LAEs such as Lyα luminosity function, SFR, stellar mass, dark matter halo mass, rest-frame optical spectroscopic properties, etc. (e.g., Guaita et al. 2011, 2013; Nilsson et al. 2011; Ciardullo et al. 2012, 2014; Nakajima et al. 2013; Trainor et al. 2016; Sobral et al. 2017; Kusakabe et al. 2018). The Lyα luminosity function and its faint-end slope are of special interest since they can serve as probes of galaxy evolution and cosmic reionization (e.g., Rauch et al. 2008; Konno et al. 2016; Zheng et al. 2017). In order to determine the faint-end slope of the Lyα luminosity function, many surveys have been carried out to detect LAEs with much fainter luminosities (e.g., Blanc et al. 2011; Ciardullo et al. 2012). Based on a deep spectroscopic survey, Cassata et al. (2011) put
strong constraints on the faint-end slope of the Ly\(\alpha\) luminosity functions at 1.95 < z < 3 and 3 < z < 4.55. They ruled out a flat slope of \(-1\) at 5\(\sigma\) and 6.5\(\sigma\) levels at these two redshift ranges and specifically obtained a slope of \(-1.6 \pm 0.12\) for the Ly\(\alpha\) luminosity function at z \(\sim\) 2.5. More recently, a wide-field (1.43 deg\(^2\)) Subaru Ly\(\alpha\) survey with an unprecedented depth obtained a much larger LAE sample of >3000 galaxies at z = 2.2 (Konno et al. 2016). This sample yields an even steeper slope of \(-1.75^{+0.10}_{-0.09}\) at z \(\sim\) 2. Later on, the steep slope was confirmed by another wide-field survey (1.43 deg\(^2\)) at similar redshifts but with shallower narrowband exposures (Sobral et al. 2017). All those surveys indicated that there are more galaxies at the faint luminosity end, and their volume densities are much higher than those with higher luminosities.

Among others, stellar mass is one of the most difficult quantities to measure owing to the faint continuum of LAEs. Usually it requires rest-frame long-wavelength optical or near-IR (NIR) photometry to determine a reliable galaxy stellar mass. For an LAE at z > 2, its rest-frame long-wavelength optical and NIR continua move to NIR or mid-IR (MIR) bands. Nonetheless, an LAE appears to be very faint in NIR and MIR. A typical LAE at z \(\sim\) 2 would have an R-band magnitude of 25.3–25.5 mag (Guaita et al. 2010; Vargas et al. 2014) and a flat spectral energy distribution (SED). Thus, its NIR or MIR magnitude will also be 25.5 mag or even fainter. There are only \~20%–30% of luminous LAEs detected at 3.6 and 4.5 \(\mu\)m in the deep Spitzer IRAC surveys (Nilsson et al. 2011). It requires a large and deep coverage in NIR or MIR to detect faint LAEs and measure their stellar masses.

Furthermore, SFR and stellar mass were found to have a tight correlation for normal star-forming galaxies, called the star formation “main sequence” (SFMS; e.g., Brinchmann et al. 2004; Elbaz et al. 2007), which defines a steady star formation mode. Starburst galaxies are located above the SFMS relation (e.g., Rodighiero et al. 2011). At high redshifts, the SFMS relation is derived mainly based on galaxies with stellar mass larger than 10\(^{10}\)\(M_\odot\) (e.g., Daddi et al. 2007; Rodighiero et al. 2011; Fang et al. 2012; Shivaei et al. 2015, 2017), and it is often extrapolated to low mass to be compared with LAEs. There is only one image with a seeing larger than 1″. The N393 imaging observations of the COSMOS and ECDF-S fields were conducted with Megacam (McLeod et al. 2015) on the 6.5 m Magellan II telescope. Megacam is a wide-field mosaic CCD camera with 9 \times 4 CCD arrays, each of which has 2048 × 4608 pixels. The focus ratio (f/5) for Megacam on Magellan leads to a pixel scale of 0.08 pixel\(^{-1}\) and thus an effective field of view of \~24′ × 24′. We used a binning of 2 \times 2 for a faster readout, yielding an actual pixel scale of 0.16 pixel\(^{-1}\). The observations were executed using a dithering mode with a single exposure of 15 minutes to minimize the number of saturated stars\(^7\) in each exposure. The dithering steps vary from \~49″ to 63″ to fill in the chip gaps. During the narrowband observations, the seeing spans a range of 0″5–1″0,\(^8\) but mostly smaller than 0″7. The resultant median seeing is 0″6. After rejecting a few raw images with unusually high sky background, we obtained total exposures of 600 and 660 minutes in the COSMOS and ECDF-S fields, respectively. The observation parameters are summarized in Table 1.

### 2. Observations and Data Reduction

#### 2.1. Observations

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#### 2.2. Data Reduction

The data reduction was performed with a combination of the IRAF mscred package and the customized package Megared developed at CfA/Harvard.\(^9\) The science images were first bias- and dark-corrected and then flat-fielded. The flat field was generated using the twilight flat taken in this run. We then removed the residual pattern in each reduced frame by subtracting each frame by the mean background frame, which was produced by stacking all science frames after removing all objects on them.

\(^7\) Stars are saturated at a narrowband magnitude of 15.4 mag.

\(^8\) There is only one image with a seeing larger than 1″0, and it was rejected.

\(^9\) https://www.cfa.harvard.edu/~mashby/megacam/
The effective coverages for the dashed lines represent the broad $U$- and $B$-band filters, respectively. The solid line represents our customized narrowband filter N393, while the dotted and dashed lines represent the broad $U$- and $B$-band filters, respectively.

The WCS solution for each science image needs to be refined based on the preliminary WCS solution assigned in the observations. We used the CIA/Harvard-developed TCL script “megawcs” to correct distortion and relative array placement of each frame. The reference positions used in this correction were those of bright objects taken from the HST/ACS $I$-band catalog in COSMOS (Capak et al. 2007; Ilbert et al. 2009) and the GEMS HST/ACS $V$-band catalog in ECDF-S (Caldwell et al. 2008). Position offsets for these objects in the refined images and the reference catalogs are plotted in Figure 2 with standard deviations of $0.016$ and $0.017$ in COSMOS and ECDF-S, respectively. The accurate WCS in each image permits optimization of the point-spread function (PSF) in the final stacked image.

The photometric zero-point in each observed frame varies owing to the changes of photometric conditions during the observations. Because we cover only one field of view with dithers in each field, we are able to use one set of bright stars in each field to normalize the zero-point in each exposure to a reference frame. A reference frame is one taken under the photometric condition with airmass $\sim1$. We measured flux densities of those bright objects in each single frame and compared them with those in the reference image. A median flux ratio was calculated for each frame, and this ratio was used to normalize the photometric zero-point of each frame to that of the reference frame before stacking. Finally, these images were mosaicked into a single frame using Swarp software (Bertin et al. 2002). A coverage map was also generated accordingly in each field. The FWHM for PSFs of the final stacked science images in both fields is $0.57''$. The effective coverages for the two fields are nearly the same, each $\sim26'9 \times 26'9$.

The absolute flux calibration was done using archival $U$- and $B$-band images in COSMOS and ECDF-S. Specifically, CFHT $u'$ and Subaru $B_1$ from the COSMOS archive$^{10}$ (Capak et al. 2007) and ESO MPG Wide Field Imager $U$- and $B$-band images from the Multiwavelength Survey by Yale-Chile (MUSYC) archive$^{11}$ (Taylor et al. 2009; Cardamone et al. 2010) were used for the COSMOS and the ECDF-S fields, respectively. The central wavelength of our N393 narrowband filter is in between the $U$ and $B$ bands, so a linear interpolation of $U$- and $B$-band fluxes at the central wavelength of N393 can be used as the underlying continuum of the Ly$\alpha$ emission (Nilsson et al. 2009; Guaita et al. 2010). Following Guaita et al. (2010), we derived the fractional contributions from $U$- and $B$-band flux densities, taking account of the central wavelengths of the filters (see Section 2.3). Finally, by assuming that the median color excess (see Section 3) of all objects is zero, the zero-point of the N393 image was derived. However, as noted by Sobral et al. (2017), a narrowband filter like ours covers the strong stellar CaHK absorption feature. A blind use of objects without considering their spectral types could introduce problems. Hence, we searched for counterparts of our narrowband-detected objects in the 3D-$HST$ catalogs (Skelton et al. 2014) and selected star-forming galaxies using the $UVJ$ method (Williams et al. 2009; Brammer et al. 2011) based on the rest-frame $U − V$ and $V − J$ colors provided by the 3D-$HST$ catalogs. It turned out that the narrowband zero-point based on star-forming galaxies is consistent with that obtained using all objects. This implies that our narrowband-detected objects are not dominated by objects with strong stellar CaHK absorption. The $5\sigma$ limiting magnitudes in a $3''$ diameter aperture in the narrowband images are $25.97$ and $26.02$ mag for the COSMOS and ECDF-S fields, respectively.

### Table 1

| Field     | R.A.$^a$ | Decl.$^a$ | Total Exposure (minutes) | PSF(FWHM) |
|-----------|---------|-----------|--------------------------|-----------|
| ECDF-S    | $3^h32^m26^s0$ | $-27\textdegree49'20''$ | 660                       | 0.6''     |
| COSMOS    | $10^h00^m27^s9$ | $+2\textdegree12'03''$  | 660                       | 0.6''     |

Note.

$^a$ This indicates the center of the pointing.

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$^{10}$ [http://irsa.ipac.caltech.edu/data/COSMOS](http://irsa.ipac.caltech.edu/data/COSMOS)

$^{11}$ [http://www.astro.yale.edu/MUSYC](http://www.astro.yale.edu/MUSYC)
2.3. Photometry

We detected objects from the narrowband image using SExtractor software (Bertin & Arnouts 1996). Objects with a minimum of 11 adjacent pixels above a threshold of 1.5σ per pixel were selected. The coverage map was used as the weight image to depress spurious detections. Aperture magnitudes with circular apertures of diameters of 8 pixels, ∼2 FWHM of seeing disks, were measured. We then made aperture corrections to obtain the total fluxes using the growth curve derived from bright stars. We note that such aperture corrections are made by assuming that the objects are point-like sources. Such an assumption is reasonable for the vast majority of our LAEs (J. S. Huang et al. 2018, in preparation). We note that MAG_AUTO from SExtractor is often used to measure the total Lyα fluxes in the literature. However, the fluxes measured by MAG_AUTO are dependent on the survey depth and are biased measurements for faint objects near the detection limits, as noted by Matthee et al. (2016) and Konno et al. (2014). This was also seen in our data. We found that the aperture-corrected fluxes underestimate the total fluxes probed by MAG_AUTO only for bright LAEs, while the MAG_AUTO fluxes for LAEs with NB > 25 mag are consistent with the aperture-corrected fluxes on average but with larger photometric errors. Therefore, we decided to use the aperture-corrected flux as a measure of the total flux in the following analysis. The exception is that MAG_AUTO was also used in the construction of Lyα luminosity functions (See Section 4) for the purpose of comparisons with studies in the literature.

Objects with signal-to-noise ratio less than 5 in the narrowband photometry were excluded. But objects fainter than the 5σ limiting magnitude were not removed from the catalog. We masked out saturated stars and high-noise area (with exposure time ≤150 minutes) in the narrowband images. The objects located in the masked area were accordingly removed from the catalog. The final narrowband photometry catalogs consist of 25,756 and 27,946 objects, covering an effective area of 602.05 and 612.75 arcmin² in the COSMOS and ECDF-S fields, respectively.

For the calculation of the narrowband-to-broadband color excess, we rebinned the U- and B-band images to match the pixel scale of the narrowband image in each field and then performed aperture photometry on the broadband images using SExtractor software in “dual-image” mode. The narrowband image was used as the detection image, and the broadband images were taken as measurement images. We used the same setup in the “dual-image” mode as that used for the source detection, as listed above. The seeing FWHMs of U- and B-band images are 0.987 and 0.994 for COSMOS and 1.03 and 1.02 for ECDF-S. Circular aperture photometry with diameters of 12 (14) pixels was carried out on both U- and B-band images for the COSMOS (ECDF-S) field. For some objects detected in the narrowband, the measured broadband fluxes have signal-to-noise ratio less than 2. We then used 2σ flux limits for these objects. Similar to the narrowband case, aperture corrections were subsequently made to measure the total fluxes using the growth curves obtained from bright stars in U and B bands. Aperture-corrected magnitudes were used to calculate the narrowband-to-broadband color excess.

After the photometry in both narrowband and its adjacent broadbands was obtained, the underlying continuum of the Lyα line, denoted by $f_{\lambda_{UB},con}$, the Lyα equivalent width (EW), and the Lyα line flux could be calculated. Since the broadband observations of the two fields used different filters, we adopted different equations to calculate these quantities. As mentioned in Section 2.2, we used a linear combination of U- and B-band flux densities to measure the continuum with the central wavelengths of the filters taken into account. Specifically, the interpolated U- and B-band flux densities at the narrowband central wavelength are derived via the linear interpolation formula

$$\frac{f_{\lambda_{UB}} - f_{\lambda_{UB},con}}{\lambda_{NB} - \lambda_{UB}} = \frac{f_{\lambda_{B}} - f_{\lambda_{UB},con}}{\lambda_{B} - \lambda_{UB}},$$

where $f_{\lambda_{UB}}$ is the interpolated U- and B-band flux density at the narrowband central wavelength, $f_{\lambda_{UB},con}$ and $f_{\lambda_{B}}$ are the U- and B-band flux densities, while $\lambda_{NB}$, $\lambda_{UB}$, and $\lambda_{B}$ are the central wavelengths of the narrowband, U-band, and B-band filters.
respectively. For COSMOS, \( f_{ UX } = 0.80 f_{ LW } + 0.20 f_{ LB } \), while for ECDF-S, \( f_{ UX } = 0.57 f_{ LW } + 0.43 f_{ LB } \). For the COSMOS field, we note that the CFHT U-band filter includes the Ly\( \alpha \) line (see the left panel of Figure 1). Therefore, we need to remove the Ly\( \alpha \) emission from the observed U-band flux density before it is used to calculate the underlying continuum. For LAEs in COSMOS, the equation used to calculate the continuum of the Ly\( \alpha \) line is

\[
 f_{ LU,UB,con } = \frac{ f_{ UX } - 0.80 f_{ LW } \Delta \lambda_{ UB } / \Delta \lambda_{ UB } }{ 1 - 0.80 \Delta \lambda_{ UB } / \Delta \lambda_{ UB } },
\]

where \( f_{ LW } \) is the narrowband flux density, while \( \Delta \lambda_{ UB } \) and \( \Delta \lambda_{ UB } \) are the bandwidth of the narrowband and U-band filters, respectively. Accordingly, the EW for LAEs in the COSMOS field can be derived using the following equation:

\[
 EW_{ obs } = \frac{ f_{ UX } - f_{ LW } }{ f_{ UX } - f_{ LW } } \times \frac{ 0.80 \Delta \lambda_{ UB } / \Delta \lambda_{ UB } }{ \Delta \lambda_{ UB } }.\]

where \( EW_{ obs } \) is the observed EW that is related to the rest-frame EW by \( EW_{ obs } = (1 + z)EW_{ rest } \). The Ly\( \alpha \) flux is obtained as follows

\[
 F(\text{Ly}\alpha) = \frac{ f_{ UX } - f_{ LW } }{ 1 - 0.80 \Delta \lambda_{ UB } / \Delta \lambda_{ UB } } \Delta \lambda_{ UB }.
\]

For the case of the ECDF-S field, the calculations of \( f_{ LU,UB,con } \), Ly\( \alpha \) EW, and Ly\( \alpha \) line flux are simpler since the Ly\( \alpha \) line is not included in the broadband filters. So for LAEs in ECDF-S,

\[
 f_{ LU,UB,con } = f_{ UX } \cdot \Delta \lambda_{ UB }, \quad EW_{ obs } = \frac{ f_{ UX } - f_{ LW } }{ f_{ UX } - f_{ LW } } \Delta \lambda_{ UB }, \quad F(\text{Ly}\alpha) = \frac{ f_{ UX } - f_{ LW } }{ 1 - 0.80 \Delta \lambda_{ UB } / \Delta \lambda_{ UB } } \Delta \lambda_{ UB }.
\]

and the Ly\( \alpha \) flux is derived using the following equation:

\[
 F(\text{Ly}\alpha) = (f_{ LW } - f_{ UX }) \Delta \lambda_{ UB }.
\]

### 2.4. Survey Completeness

It is essential to determine the completeness of the narrowband surveys. The Monte Carlo simulations were employed to measure the narrowband survey completeness in both fields. We first selected several tens of bright stars (SExtractor parameter \( \text{CLASS} \star \geq 0.95 \)) with the aperture-corrected narrowband magnitudes 19 mag \( \leq NB < 22 \) mag in both fields, scaled down their flux densities, and put back in random locations in their original images. SExtractor with the same parameter set was run again on the images with artificial objects. This simulation was performed several hundred times to achieve adequate statistics in each magnitude bin. Completeness of the narrowband detections in both fields was measured as the artificial object recovery rate in each magnitude bin, shown as the filled data points in Figure 3. The 90% and 50% completeness limits are 25.50 and 25.99 mag for the COSMOS field and 25.78 and 26.20 mag for the ECDF-S field.

### 3. Selection of LAE Candidates

Selection of LAEs is generally based on their emission line EW. Practically the narrowband-to-broadband color excess (i.e., magnitude difference) can be used as a proxy. We use UB as magnitude for the interpolated U- and B-band flux density, and NB as narrowband magnitude. The median NB–UB should be zero for galaxies with no line shifting to the band. When a line shifts to the narrowband, the NB–UB appears \( \text{“blue”} \). We plot NB–UB against NB in Figure 4. The scatters in NB–UB come from the NB, U-band, and B-band photometry uncertainties. We measured the rms scatters \( \sigma_{ NB,UB } \) in the NB–UB distributions as a function of NB magnitude and used 3\( \sigma_{ NB,UB } \) as the threshold to select narrowband-excess sources as LAE candidates. Due to the different depths in broadband photometry in these two fields, EWs calculated using 3\( \sigma_{ NB,UB } \) are slightly different, ~20 \( \AA \) in COSMOS and ~30 \( \AA \) in ECDF-S. If a selection criterion of EW \( \geq 30 \) \( \AA \) is used for COSMOS, the number densities and main results do not change significantly (see below for details). This selection left us with 212 LAEs in COSMOS and 263 LAEs in ECDF-S, shown in Figure 4.

The narrowband-excess sample yielded by the single NB–UB selection also includes objects with emission lines other than the Ly\( \alpha \) line redshifting to our narrowband filter waveband, for example, [O II] at \( z \approx 0.05 \), [Al III] at \( z \approx 1.1 \), [C III] at \( z \approx 1.06 \), [C IV] at \( z \approx 1.5 \), [Si IV] + [O IV] at \( z \approx 1.8 \), etc. Among these lines, only [O II] appears in a normal galaxy spectrum, while the remaining high-ionization lines appear in active galactic nucleus (AGN) spectra. The [O II] emitters are at such a low redshift that they occupy too small a volume to actually contribute to the selected sample. Those high-ionization line emitters were identified using X-ray catalogs (Lehmer et al. 2005; Virani et al. 2006; Luo et al. 2008; Civano et al. 2012) and spectroscopic information from NED.12 We identified 16 broad-line AGNs and one candidate AGN with X-ray emission at \( z = 1.694 \) (Salvato et al. 2011) in COSMOS and seven broad-line AGNs in ECDF-S in the narrowband-excess sample. Four of the broad-line AGNs in COSMOS (Trump et al. 2009; Civano et al. 2012) and two in ECDF-S.

12 http://nedwww.ipac.caltech.edu/
Treister et al. (2009; Silverman et al. 2010) have spectroscopic redshifts of \( \sim 2.23 \). For the study of the Ly\( \alpha \) luminosity functions in Section 4, we include these \( z \sim 2.23 \) broad-line AGNs and reject all the other AGNs. But for the study of star formation properties of LAEs, all broad-line AGNs are removed. The other possible contamination sources are Lyman break galaxies (LBGs) at \( z \sim 3 \). At \( z \sim 3 \), both the narrow band and broad \( B \) band sample the continuum at rest-frame wavelength longer than 912 Å, while the \( U \) band samples the rest-frame flux shorter than 912 Å. The break makes interpolation between \( U \) and \( B \) band artificially low, and \( NB-UB \) appears to be excessive. We simply use \( NB-B \) color to reject \( z \sim 3 \) LBGs. The reliability of this criterion was tested by LBGs selected by the classical LBG technique. Specifically, we apply the criteria proposed by Álvarez-Márquez et al. (2016) to select \( z \sim 3 \) LBGs in our COSMOS field using the COSMOS public archival catalog and the criteria adopted by Hildebrandt et al. (2005) to select \( z \sim 3 \) LBGs in our ECDF-S field using the MUSYC public catalog. As shown in Figure 5, LBGs mostly have \( NB-B \geq 0 \) and LAEs have \( NB-B < 0 \), although a minority of LBGs have \( NB-B < 0 \). A more strict criterion of \( NB-B \geq -0.3 \) would not change our results significantly. This criterion only identifies five \( z \sim 3 \) LBGs in COSMOS that were rejected from the sample. The final sample consists of 194 LAE candidates (including four AGNs) in COSMOS and 258 LAE candidates (including two AGNs) in ECDF-S.

Both EW and narrowband flux limit have selection effects in a narrowband-excess-selected LAE sample. Figure 6 shows that our sample does not include LAEs with low Ly\( \alpha \) luminosity and high EW. This results from the narrowband detection limits. An LAE with low Ly\( \alpha \) luminosity and high EW implies a low continuum; therefore, its narrowband flux, i.e., the sum of the emission-line flux and the continuum, is too low to be detected in the narrowband imaging (Graur et al. 2010). From Figure 6, we also see that a larger number of faint LAEs were selected in ECDF-S than in COSMOS because of the deeper narrowband exposure in the ECDF-S.
Selection effects in the COSMOS (red circles) and ECDF-S (blue triangles) fields shown in the rest-frame EW vs. logarithmic Lyα luminosity plot. The red and blue horizontal lines indicate the color excess selection threshold for the two fields that are equivalent to Lyα EW of 20 and 30 Å for the COSMOS and ECDF-S fields, respectively. The red and blue solid curves correspond to the faintest narrowband magnitude in the COSMOS and ECDF-S LAE samples, respectively.

The different selection criteria in EW employed by these two fields are also clearly seen in this figure. There are 31 LAEs with rest-frame EW between 20 and 30 Å in COSMOS, ∼16% of the LAE sample in COSMOS. However, the inclusion of these LAEs compared to a selection criterion of EW ≥ 30 Å does not change the number densities per luminosity bin significantly, due to the wide spread of these LAEs in the Lyα luminosity as shown in Figure 6. The changes are mostly within the 1σ Poisson noises.

4. LAE Number Counts and Lyα Luminosity Function

Measurement of galaxy number counts is a direct way of estimating the depth of an imaging survey. We use Lyα magnitude/flux (with continuum subtracted; see Equations (4) and (7)) to perform the analysis. The Lyα magnitude m(Lyα) is linked to the Lyα flux via the equation m(Lyα) = −2.5 log (F(Lyα) × $10^{-20}$ erg s$^{-1}$ cm$^{-2}$) + m$_0$, where c is the speed of light and m$_0$ is the zero-point of the AB magnitude system. The LAE number counts of the COSMOS and ECDF-S fields are listed in Table 2. In Figure 7, we plot our counts against those in previous narrowband surveys with publicly available catalogs at similar redshifts. It shows that our counts reach a limiting magnitude of 1.58 × 10$^{-17}$ erg s$^{-1}$ cm$^{-2}$. It is clear from Figure 7 that most surveys have consistent number counts up to F(Lyα) = 2.5 × 10$^{-17}$ erg s$^{-1}$ cm$^{-2}$, but at the faintest luminosity bin of F(Lyα) = 1.58 × 10$^{-17}$ erg s$^{-1}$ cm$^{-2}$, our survey has the highest counts compared with previous surveys (Nilsson et al. 2009; Mawatari et al. 2012). Note that the narrowband imaging completeness-corrected LAE number counts of the COSMOS and ECDF-S fields are different at the faintest end. This may be caused by different narrowband depths in the two fields and potential uncertainties associated with the large completeness correction in COSMOS at the faintest magnitude bin, as shown in Figures 6 and 3, respectively.

With the deep LAE sample, we estimated the Lyα luminosity function with the $(1/V_{max})$ method (Shimasaku et al. 2006; Gronwall et al. 2007; Ouchi et al. 2008; Hu et al. 2010; Konno et al. 2016). For a boxcar-shaped narrowband filter, it would be straightforward to derive the luminosity function by simply dividing the observed incompleteness-corrected number counts by their effective volume, i.e., the classical method (e.g., Shimasaku et al. 2006; Ouchi et al. 2008). However, in reality...
the narrowband filter transmission curve does not have a boxcar shape, and the classical method suffers from some uncertainties, as noted by Ouchi et al. (2008). Ouchi et al. (2008) showed that these uncertainties are not important and, or cancel each other, but this may not apply to our samples owing to the different filter shapes and survey properties. Unfortunately, the sample sizes and the narrow coverage in Ly$\alpha$ luminosity do not allow us to perform a sophisticated simulation like Ouchi et al. (2008).

Hence, we assume that the potential uncertainties caused by our non-boxcar filter profile cancel each other too.

Under the assumption that the redshift range corresponds to the FWHM of the narrowband filter, the effective comoving volumes probed by our narrowband surveys for COSMOS and ECDF-S fields are $1.16 \times 10^5$ Mpc$^3$ and $1.18 \times 10^5$ Mpc$^3$, respectively. The derived Ly$\alpha$ luminosity functions are provided in Table 3 and shown in Figure 8. The completeness at $L(Ly\alpha) < 10^{41.8}$ erg s$^{-1}$ is lower than 20%. We do not use LAEs below $10^{41.8}$ erg s$^{-1}$ in the estimation of the luminosity functions. The errors include uncertainties from both Poisson noise (Gehrels 1986) and cosmic variance. Following the method in Konno et al. (2016), the cosmic variance uncertainty is obtained from the bias factor of our LAEs derived in Section 5.3 and the dark matter density fluctuation in a sphere with a radius of $\sim 30$ Mpc (corresponding to our survey volume) at redshift 2.23. For both fields, the resultant cosmic variance uncertainty is 17.7%.

As can be seen in Figure 8, our Ly$\alpha$ luminosity functions of the two fields agree with each other and are generally consistent with those obtained in previous surveys (Hayes et al. 2010; Blanc et al. 2011; Cassata et al. 2011; Ciardullo et al. 2012; Konno et al. 2016). We specifically compare our results with the recent work by Konno et al. (2016) and Sobral et al. (2017). For a better comparison, apart from the best-fit luminosity functions, data points from Sobral et al. (2017) and data points with $L(Ly\alpha) > 10^{43}$ erg s$^{-1}$ from Konno et al. (2016) are also plotted in Figure 8.

Both surveys observed an effective area of 1.43 deg$^2$ and probe a comoving volume of $1.32 \times 10^6$ Mpc$^3$ (Konno et al. 2016) and $7.3 \times 10^5$ Mpc$^3$ (Sobral et al. 2017), respectively. The limiting Ly$\alpha$ luminosities are $10^{41.7}$ erg s$^{-1}$ for Konno et al. (2016) and $10^{42}$ erg s$^{-1}$ for Sobral et al. (2017). Although these surveys probe much larger areas and comoving volumes than ours, we reach a comparable depth of Ly$\alpha$ luminosity limit of $10^{41.8}$ erg s$^{-1}$ with Konno et al. (2016) in the luminosity functions. Sobral et al. (2017) have made extensive comparisons with Konno et al. (2016). They showed that when the same EW threshold was used and no contaminants were removed, their Ly$\alpha$ luminosity function would be perfectly consistent with Konno et al. (2016). Even without matching the selection criteria, their results are claimed to be in good agreement with Konno et al. (2016) over most luminosities. Our luminosity functions roughly follow the trend of them, but the volume densities are systematically lower at $L(Ly\alpha) < 10^{43}$ erg s$^{-1}$. The possible causes for the differences are twofold. One is the measurement of the total luminosity. We used aperture-corrected fluxes to probe the total flux, while Konno et al. (2016) used MAG_AUTO and Sobral et al. (2017) used a larger aperture to measure the total flux. The other is the completeness correction. We used bright stars to evaluate the detection completeness and assumed that effects caused by our non-boxcar filter profile cancel each other, similar to Konno et al. (2016). But Sobral et al. (2017) performed more

Table 3

| log $[L(Ly\alpha)]$ | $\Phi$ (COSMOS)$^a$ | $\Phi$ (ECDF-S)$^a$ | $\Phi$ (COSMOS)$^b$ | $\Phi$ (ECDF-S)$^b$ |
|-------------------|------------------|------------------|------------------|------------------|
| (erg s$^{-1}$)    | (10$^{-4}$ Mpc$^3$ log$L$) | (10$^{-4}$ Mpc$^3$ log$L$) | (10$^{-4}$ Mpc$^3$ log$L$) | (10$^{-4}$ Mpc$^3$ log$L$) |
| 41.90             | 28.44$^{+6.32}_{-6.28}$ | 33.05$^{+12.26}_{-12.01}$ | 53.49$^{+12.26}_{-12.01}$ | 49.11$^{+10.41}_{-10.41}$ |
| 42.10             | 19.94$^{+4.99}_{-4.57}$ | 19.55$^{+5.63}_{-5.19}$ | 21.51$^{+5.63}_{-5.19}$ | 19.88$^{+5.08}_{-4.71}$ |
| 42.30             | 13.36$^{+3.36}_{-3.14}$ | 12.29$^{+4.95}_{-4.29}$ | 17.94$^{+4.95}_{-4.29}$ | 11.88$^{+4.36}_{-4.09}$ |
| 42.50             | 6.03$^{+3.24}_{-2.38}$ | 6.36$^{+2.98}_{-2.58}$ | 9.23$^{+2.98}_{-2.58}$ | 8.50$^{+2.80}_{-2.41}$ |
| 42.70             | 2.16$^{+1.01}_{-1.01}$ | 1.27$^{+1.71}_{-1.24}$ | 3.20$^{+1.71}_{-1.24}$ | 1.27$^{+1.26}_{-1.03}$ |
| 42.90             | 0.86$^{+0.15}_{-0.08}$ | 1.69$^{+1.17}_{-0.88}$ | 1.72$^{+1.17}_{-0.88}$ | 1.69$^{+1.37}_{-0.88}$ |
| 43.10             | 0.86$^{+0.15}_{-0.08}$ | 0.42$^{+0.98}_{-0.58}$ | 0.86$^{+1.15}_{-0.58}$ | 1.27$^{+1.26}_{-0.73}$ |
| 43.30             | 0.86$^{+0.15}_{-0.08}$ | 0.86$^{+0.98}_{-0.58}$ | 0.86$^{+1.15}_{-0.58}$ | 1.27$^{+1.26}_{-0.73}$ |
| 43.50             | 0.86$^{+0.15}_{-0.08}$ | 0.86$^{+0.98}_{-0.58}$ | 0.86$^{+1.15}_{-0.58}$ | 1.27$^{+1.26}_{-0.73}$ |

Notes.

$^a$ Aperture-corrected fluxes and completeness curves based on bright stars are used.

$^b$ Fluxes represented by MAG_AUTO and completeness curves derived with the reconstructed narrowband image of our LAEs are used.

Figure 8. Comparisons of $z \sim 2$ Ly$\alpha$ luminosity functions in this work and those in the literature. The big data points represent our observed luminosity functions derived using aperture-corrected fluxes and star-based completeness curves for the COSMOS (red circles) and ECDF-S (blue triangles) fields. The color-coded curves show luminosity functions by different groups, as labeled in the upper right corner. Data points from Sobral et al. (2017) and the data points with $L(Ly\alpha) > 10^{43}$ erg s$^{-1}$ from Konno et al. (2016) are plotted as small green stars and small brown filled circles, respectively.
corrections, including both selection completeness and filter profile biases.

To understand our systematically lower number densities than Konno et al. (2016) and Sobral et al. (2017), we derive Ly$\alpha$ luminosity functions using MAG\_AUTO as a measure of the total flux and completeness curves built on a reconstructed LAE narrowband image. The reconstructed LAE narrowband image is obtained by stacking the narrowband images of our LAEs. The approach used to construct the completeness curves is similar to that using bright stars in Section 2.4. The difference is that the reconstructed and flux-scaled LAE narrowband images are used as the input fake narrowband images and MAG\_AUTO is used to measure the flux of the fake objects. The stacked LAE for each field has an FWHM of $\sim 0.9''$, slightly broader than the PSF. It is the requirement of the recovery (within 3$\sigma$) of the input MAG\_AUTO that makes the detection completeness different from the ones using bright stars and aperture-corrected magnitudes, as shown in Figure 3. The resultant Ly$\alpha$ luminosity functions are added to Table 3 and shown in Figure 9. The luminosity functions based on aperture-corrected fluxes and completeness curves derived with stars are overplotted as gray open points for comparison. As can be seen, our results based on MAG\_AUTO and completeness from the reconstructed LAE narrowband image agree well with the Ly$\alpha$ luminosity function of Sobral et al. (2017), although the number densities are still slightly lower than those of Konno et al. (2016). Virtually, the offsets between the Ly$\alpha$ luminosity functions based on our two methods are mostly within 1$\sigma$ uncertainties as seen from Figure 9. The number densities based on the aperture-corrected fluxes and completeness derived using stars are systematically low though, The main contributor of the systematics comes from the completeness correction. This is especially the case for the faint part, as clearly shown in Figure 3. Therefore, we caution that systematics potentially introduced by different methods should be considered when Ly$\alpha$ luminosity functions from different studies are compared. Although number densities are affected by completeness corrections, the slope of our Ly$\alpha$ luminosity functions at the faint end is consistent with Konno et al. (2016) and Sobral et al. (2017), regardless of the use of measures of total fluxes and completeness curves.

Regarding the bright end ($L(Ly\alpha) > 10^{42}$ erg s$^{-1}$) of the luminosity functions, our results are consistent with Konno et al. (2016) but show higher volume densities than Sobral et al. (2017), as shown in both Figures 8 and 9. The use of MAG\_AUTO and completeness curves based on the reconstructed LAE narrowband image does not change our bright-end luminosity functions dramatically. Sobral et al. (2017) claimed that the higher volume densities at the bright end in Konno et al. (2016) are caused by contaminations from non-LAE AGNs. Our AGNs are spectroscopically confirmed $z \sim 2.23$ LAEs, so our higher volume densities than Sobral et al. (2017) are real. But we note that the bright-end luminosity functions suffer from small number statistics. There are typically one to two objects in each bin. Virtually, the figures show that the bright-end difference between our data points and the results in Sobral et al. (2017) is mostly within 1$\sigma$ errors. Furthermore, the cosmic variance uncertainties are probably underestimated since AGNs have much larger bias factor than our LAEs (Allevato et al. 2011). The actual error bars should be even larger, which would lead to a conclusion that the bright end of our Ly$\alpha$ luminosity functions is consistent with that of Sobral et al. (2017) within 1$\sigma$ uncertainties.

5. LAEs as Low-mass Galaxies at $z \sim 2.23$

The universe was in a critical epoch at $z \sim 2$ when SFR density reached the highest point. Most studies at this redshift focused on massive galaxies. Low-mass galaxies are also important in constraining galaxy formation models. Yet it is quite challenging to identify low-mass galaxies at high redshifts. The narrowband technique provides an effective way to detect LAEs with very low stellar masses at high redshifts. However, only a small fraction of them are detected in longer-wavelength bands (e.g., Nilsson et al. 2011), making it hard to estimate their stellar population parameters. We specifically chose both COSMOS and ECDF-S fields where deep ancillary photometry data, especially deep Spitzer/IRAC observations, are available. Therefore, we are able to study the properties of low-mass galaxies at $z \sim 2$ by investigating their stellar population, star formation properties, and dark matter halo mass.

5.1. Stellar Population and Stellar Mass Function

The SEDS (Ashby et al. 2013) reaches limiting flux densities of sub-microjansky in 3.6 and 4.5 $\mu$m for COSMOS and ECDF-S, providing critical constraints on stellar mass measurements for faint LAEs in these two fields. Out of the 446 sample non-AGN LAEs, 130 ($\sim 29\%$) were detected in the SEDS imaging, which include 96 ($\sim 38\%$) LAEs in the ECDF-S field and 34 ($\sim 18\%$) LAEs in the COSMOS field. The different SEDS detection fractions in COSMOS and ECDF-S are due to the fact that SEDS only covers a part (10$''$ × 60$''$ strip) of our narrowband observed area in COSMOS. For the 130 IRAC-detected LAEs, we estimated their stellar masses using the SED fitting software FAST (Kriek et al. 2009). Multimwavelength SEDs were constructed as follows: The optical and NIR data are retrieved from MUSYC (Cardamone et al. 2010), GEMS (Rix et al. 2004),
Taiwan ECDFS Near-Infrared Survey (TENIS; Hsieh et al. 2012), COSMOS (Capak et al. 2007), and SEDS (Ashby et al. 2013). Specifically, MUSYC U and B bands, GEMS F606W and F850LP bands, TENIS J and Ks bands, and SEDS 3.6 and 4.5 μm are used for the ECDF-S field, while u′, B, V, r′, i′, z′, and Ks bands from the COSMOS photometry catalog and SEDS 3.6 and 4.5 μm are used for the COSMOS field.13 The stellar population synthesis models of Bruzual & Charlot (2003) were adopted, assuming a Salpeter IMF, an exponentially declining star formation history, and a stellar metallicity of 0.2 Z⊙. For dust attenuation modeling, the Calzetti dust extinction law (Calzetti et al. 2000) was used. Figure 10 shows examples of our SED fitting for two IRAC-detected LAEs. We note that Hα emission contributes to the Ks-band flux densities that would potentially bias the stellar mass estimates. Hence, we performed SED fitting without using Ks-band data and found that the stellar masses do not change much. In other words, no systematic biases were introduced by including Ks band in the SED fitting. The stellar masses were mainly constrained by the SEDS MIR data.

Our SED fitting results show that the stellar masses for most IRAC-detected LAEs are in the range of 8 < log(M*/M⊙) < 10, but there do exist massive LAEs with stellar mass larger than 10^{10} M⊙, even more massive than 10^{11} M⊙. On the other hand, for IRAC-undetected LAEs, we used stacking analysis to derive a median SED. As mentioned above, SEDS only covers a part of our narrowband imaging survey area for COSMOS. To achieve high signal-to-noise ratio, we only used IRAC-undetected LAEs in ECDF-S for the stacking analysis. The stacked IRAC 3.6 and 4.5 μm magnitudes for the IRAC-undetected LAEs are 26.93 ± 0.09 mag and 27.02 ± 0.14 mag, respectively, which are similar to the stacking result for LAEs at z ≈ 3.1 (Lai et al. 2008). Figure 11 presents the median-stacked SED along with the best fit, which yields a stellar mass of log(M*/M⊙) = 7.97 ± 0.05 and dust extinction of A_V = 0.12 ± 0.05 mag. This is among the lowest mean stellar masses compared to the LAE samples in previous studies (Hagen et al. 2014, 2016; Vargas et al. 2014). In Figure 11, we note that the B-band photometry is far above the best fit, but we cannot figure out the reason for this unreasonably high flux. Fortunately, the stellar mass and dust attenuation are not affected by this photometric data point. If B-band photometry is not included in the SED fitting, the results only change within 1σ errors.

13 For some LAEs, there are no photometric data available in a few required wavebands. But the remaining waveband data, especially the crucial MIR bands, provide reasonable constraints on the SED shapes and hence the stellar masses.

Although LAEs may just be one of the high-redshift galaxy populations with log(M*/M⊙) ∼ 8, there are few studies on galaxies with such a low stellar mass at z ∼ 2 besides LAEs, and thus poor constraints on the low-mass end of the stellar mass function. With the estimation of a median stellar mass of \(10^8 M_\odot\) from the IRAC-undetected LAEs, we can have a rough estimation of their number density. This was simply done by dividing the number of IRAC-undetected LAEs by the product of the effective comoving volume and the stellar mass range, without any corrections. Since stellar mass cannot be derived for IRAC-undetected LAEs individually, the stellar mass range cannot be estimated in the normal way. Instead, we estimated the stellar mass range via the SFR range. The stellar mass range in log-space is equal to the logarithmic SFR range under the assumption that the specific SFRs (i.e., SFR/M_*) of these IRAC-undetected LAEs are the same. We estimated the SFR range covered by the IRAC-undetected LAEs using the rest-frame UV-derived SFRs (see Section 5.2) of these LAEs and obtained a number density of log(Φ/Mpc^{-3} dex^{-1}) = −3.0 at log(M*/M⊙) = 8. We note that the number density derived this way suffers from large uncertainties introduced by the sample incompleteness and the assumption made in deriving the stellar mass range. It is probably a lower limit of the real number density considering the sample incompleteness. But it is still worth examining its position on the stellar mass function diagram given its low stellar mass.
Figure 12. Stellar mass functions at \( z \sim 2 \). The red circle represents the constraints from our IRAC-undetected LAEs. The smaller error bars indicate the 1\( \sigma \) errors from the SED fitting, while the larger error bars reflect the possible rms scatter in the stellar mass distribution of the IRAC-undetected LAEs, derived from the rms scatter in the SFRs of these LAEs by assuming that their specific SFRs are the same. Deep stellar mass functions from recent studies as indicated in the lower right corner are shown for comparison.

Figure 12 shows the derived number density of our IRAC-undetected LAEs in the stellar mass function diagram, in comparison with the existing stellar mass functions at redshift \( z \sim 2 \) (Reddy & Steidel 2009; Santini et al. 2012; Ilbert et al. 2013; Muzzin et al. 2013; Tomczak et al. 2014; Mortlock et al. 2015). As can be seen from Figure 12, the only number density measurements to \( \log(M_*/M_\odot) = 8 \) are based on the BX redshift sample (Reddy & Steidel 2009) and are much lower than ours. All photometric redshift samples at \( z \sim 2 \) are not deep enough to reach this mass limit. However, these stellar mass functions at \( \log(M_*/M_\odot) = 9.5 \) are already a factor of \( \sim 4–5 \) higher than our LAE at \( \log(M_*/M_\odot) = 8 \). Therefore, our estimation provides a lower limit for the mass function at this mass limit.

If the extrapolation of the previous stellar mass functions to the low-mass end traces the real stellar mass function, we must answer the following question: which types of galaxies compose the low-mass galaxy population? Besides the LAEs, possible populations are galaxies with a large amount of dust, galaxies that have been quenched, or genuine star-forming galaxies with a large amount of dust/cold gas geometries and orientations preventing Ly\( \alpha \) photons from escaping the galaxies. However, dusty galaxies tend to be massive (e.g., Whitaker et al. 2012, 2014), and thus it is impossible for them to be a major population at the low-mass end of the stellar mass function. On the other hand, it is also unlikely that the quenched galaxies dominate the low-mass end of the stellar mass function (e.g., Tomczak et al. 2014). The most possible missing low-mass galaxies are star-forming galaxies with interstellar medium geometries and orientations against the escape of Ly\( \alpha \) photons. It is difficult to identify the fraction of such galaxies at the moment because of their faint continuum. Future deep observations in NIR/MIR by the James Webb Space Telescope (Kalirai 2018) may shed light on this.

5.2. Star Formation Properties

The SFMS relation and its extrapolation toward the low-mass end have been widely used to characterize the star formation mode of LAEs. However, agreement has not been reached on the locations of LAEs relative to the SFMS relation (Guaita et al. 2013; Hagen et al. 2014, 2016; Vargas et al. 2014; Oteo et al. 2015; Shimakawa et al. 2017; Kusakabe et al. 2018). Differences in the narrowband survey depths and the adoption of extinction curves may be responsible for the discrepancy (Shimakawa et al. 2017; Kusakabe et al. 2018). Given that our survey is among the deepest narrowband surveys and our sample is the largest LAE sample with individual stellar mass measurements, it is worth revisiting the SFMS relation based on our LAE sample.

The rest-frame far-UV (FUV) luminosity is the most commonly used SFR tracer at high redshifts. We calculated the rest-frame FUV luminosities for our sample LAEs from the observed \( B \)-band flux densities. Then, the FUV luminosities were converted to SFRs using a conversion factor derived using STARBURST99 version 7.0.1 (Leitherer et al. 1999, 2010, 2014; Vázquez & Leitherer 2005) synthesis models for a constant star-forming population with age of 100 Myr and 0.2 \( Z_\odot \) stellar metallicity:

\[
\text{SFR}(M_\odot \text{ yr}^{-1}) = 1.35 \times 10^{-28} L_{\text{FUV}} (\text{erg s}^{-1} \text{Hz}^{-1}).
\]  

(8)

Dust attenuations were not accounted for in the SFRs derived here. The dust-uncorrected SFRs for IRAC-detected LAEs in both COSMOS and ECDF-S are in the range of 0.1 \( M_\odot \) \( \text{yr}^{-1} \) < SFR < 10 \( M_\odot \) \( \text{yr}^{-1} \), while for the LAEs without IRAC detections, the median SFR is log (SFR/\( M_\odot \) \( \text{yr}^{-1} \)) = −0.14 with an rms scatter of 0.35 dex. In addition, six massive LAEs with stellar masses of \( \sim 10^{11} M_\odot \) in the two fields are detected at MIPS 24 \( \mu \text{m} \) or even at Herschel far-IR (FIR) bands. We calculated their SFRs using the MIPS 24 \( \mu \text{m} \) flux densities (Rieke et al. 2009), which are so high that they are qualified as luminous infrared galaxies (LIRGs) or even ultraluminous infrared galaxies (ULIRGs). Considering the large PSFs of the MIR/FIR images, we inspected the Spitzer/IRAC 3.6 \( \mu \text{m} \) and MIPS 24 \( \mu \text{m} \) images for these six LAEs and confirmed that their high MIR emissions are not from contaminations by neighboring bright objects.

The left panel of Figure 13 shows the locations of our sample LAEs on the dust-uncorrected SFR versus stellar mass diagram. The red filled circles and blue filled triangles represent LAEs in the COSMOS and ECDF-S fields, respectively, while the large red and blue inverted triangles denote the MIR/FIR-detected LAEs in the respective fields. For comparison, we also plot \( z \sim 2 \) BzK-selected galaxies with dust-corrected SFRs (Rodighiero et al. 2011), \( H\alpha \) emitters with dust-corrected SFRs (HAEs; An et al. 2014) and the 50 LAEs in Shimakawa et al. (2017) with dust-uncorrected SFRs. The widely used \( z \sim 2 \) SFMS relations from Daddi et al. (2007) and Shrivei et al. (2015) are overplotted in this figure. It is clear from the left panel of Figure 13 that the majority of our IRAC-detected LAEs and the stacked IRAC-undetected LAEs are located on the SFMS relations or their extrapolations toward the low stellar mass end, within 1\( \sigma \) scatters (0.3 dex). In addition, the six MIR/FIR-detected massive LAEs with high SFRs are also on the SFMS relation and mix with the BzK-selected galaxies. The left panel of Figure 13 also shows that our 130 IRAC-detected LAEs are well mixed with the 50 LAEs of Shimakawa et al. (2017). Nevertheless, we note that as the stellar mass increases, the fraction of LAEs below SFMS also increases. Especially, as the stellar mass is larger than a few times...
10^9 M_☉, almost all LAEs are below the SFMS line. It may imply that more massive LAEs tend to be dustier and dust attenuation corrections are necessary for LAEs.

Currently, dust attenuations for LAEs are derived from SED fitting or from the UV slope (f_β ∝ λ^β). Given that the color excess E(B − V) derived via SED fitting is affected by the stellar mass (Shivaei et al. 2015), we estimate E(B − V) from the UV slope β in this work. The UV slope β could be determined reasonably well if several wavebands of data covering the rest-frame 1300–2600 Å are available. This wavelength range corresponds to the B, V, R, and I bands for objects at z ∼ 2.23. For the 34 IRAC-detected LAEs in the COSMOS field, 33 are in the COSMOS public catalog and have deep B, V, R, and I-band photometry. The six MIR/FIR-detected LAEs are included in the subsample with B, V, R, and I-band photometry. We obtained β by fitting a power law to the four bands’ flux densities via chi-square minimization. After excluding the six MIR/FIR-detected LAEs and LAEs with unreliable β measurements, we were left with 27 LAEs in COSMOS and 51 LAEs in ECDF-S with reliable β. The uncertainties in β vary from 2% to 49% and have been incorporated into the total error budget in dust-corrected SFRs subsequently. The Calzetti extinction law (Calzetti et al. 2000) was then used to calculate E(B − V) from β under the assumption that the intrinsic UV slope β_0 is −2.23 (Meurer et al. 1999). For objects with β < −2.23, zero dust extinctions were assumed. Figure 14 shows the distributions of β with a median of −1.8 for the 78 IRAC-detected LAEs with B, V, R, and I measurements. As can be seen, there are 15 LAEs with β < −2.23 and hence zero dust extinctions. Figure 14 also reveals a broad distribution in β for LAEs in both fields, which leads to a wide range of E(B − V) varying from 0 to 0.3 mag, with a median value of 0.1 mag. Using the E(B − V), we obtained the dust-corrected SFRs for the 78 IRAC-detected LAEs spanning a range of 1 M_☉ yr^{-1} < SFR < 100 M_☉ yr^{-1}. It should be noted that due to the lack of B, V, R, and I photometry, dust corrections were not performed for 39 IRAC-detected LAEs. The 39 LAEs have lower dust-uncorrected SFRs than most of the LAEs that have B, V, R, and I measurements.

The right panel of Figure 13 presents the 84 LAEs with dust-corrected SFRs, including the six MIR/FIR-detected LAEs whose SFRs were calculated from 24 μm fluxes and the 15 LAEs with zero dust extinctions. The LAEs in Shimakawa et al. (2017) are also plotted with dust-corrected SFRs. The symbols are the same as those in the left panel of Figure 13.
Note that we also plot the 39 LAEs without dust corrections for their SFRs in the figure by filled gray circles or triangles. As shown in the right panel of Figure 13, most LAEs with dust-corrected SFRs are located along the SFMS within 1σ scatter, although a small fraction of LAEs are located above the SFMS, indicating that they are in active star formation mode. As for the stacked IRAC-undetected LAEs, we do not perform dust corrections because they have minor dust attenuation as derived from the SED fitting. It is obvious that these low-mass LAEs sit on the low-mass extrapolations of the SFMS. On the other hand, the LAEs with stellar mass larger than $10^{10} M_\odot$, along with the MIR/FIR-detected (U)LIRG-like LAEs, are on the SFMS as well. In summary, LAEs are heterogeneous populations that have stellar masses and SFRs covering more than three orders of magnitude, i.e., $8 < \log(M_*/M_\odot) < 11.5$, $1 M_\odot \text{yr}^{-1} < \text{SFR} < 2000 M_\odot \text{yr}^{-1}$, and suffer from dust extinctions spanning a wide range. However, LAEs are mostly low-mass star-forming galaxies, and they follow the SFMS relations defined by massive normal star-forming galaxies and their extrapolations to the low-mass regime. This suggests that they are normal star-forming galaxies, instead of a special galaxy population in terms of star formation modes. It is unusual that an LAE is massive and MIR/FIR luminous, since even a small amount of dust could stop Ly$\alpha$ photons from escaping the galaxy. Such dusty, massive LAEs may have special dust/gas geometries favoring the escape of Ly$\alpha$ photons, as suggested by studies on Ly$\alpha$ and optical emission line profiles from local ULIRGs (Martin et al. 2015).

In the literature, different conclusions have been drawn on the relations of LAEs with respect to the SFMS. Survey depths and use of extinction curves have been proposed to be the causes. Since Shimakawa et al. (2017) have comparable narrowband survey depth with ours, we overplotted their LAEs with and without dust attenuation corrections in SFRs in the left and right panels of Figure 13 for comparison. We can see from the left panel of Figure 13 that the two LAE samples cover almost the same range in both the stellar mass and the dust-uncorrected SFR. Virtually, the two sample LAEs are mixed together in the dust-uncorrected SFR versus stellar mass diagram. On the other hand, the right panel of Figure 13 shows that the LAEs from the two samples are mostly mixed well, except a lack of our LAEs in the low-SFR part, which is caused by the absence of broad $B_{\alpha}$, $V$, $R$, and $I$-band photometry for low-SFR objects. Furthermore, we inspected Figure 9 of Hagen et al. (2014), who studied LAEs with high Ly$\alpha$ luminosities ($L(\text{Ly}\alpha) > 10^{43}$ erg s$^{-1}$), at which there are almost no LAEs below the SFMS line. In comparison with the right panel of Figure 13 in this work, the absence of LAEs below the SFMS in Hagen et al. (2014) seems to be caused by the selection effect that relatively shallow narrowband surveys leave out galaxies with lower SFRs, as pointed out by Oyariniz et al. (2017). Regarding the adoption of extinction laws, both Shimakawa et al. (2017) and this work use the Calzetti extinction curve and find that the LAEs are not significantly above the SFMS relations in the dust-corrected SFR versus stellar mass diagram. Therefore, it seems that it is not a necessity to employ a different extinction law.

5.3. Dark Matter Halo Mass

In the ΛCDM paradigm, galaxies form in dark matter halos, and galaxy evolution is closely linked to its hosting dark matter halo mass. In this subsection, we derive the dark matter halo mass for our LAEs. The bias factor and dark matter halo mass of our LAE sample were estimated via clustering analysis following Gualia et al. (2010) and Kusakabe et al. (2018). First, we calculated the angular two-point correlation function using the Landy–Szalay estimator (Landy & Szalay 1993):

$$w(\theta) = \frac{DD(\theta) - 2DR(\theta) + RR(\theta)}{RR(\theta)},$$

where DD, DR, and RR are the normalized counts for data–data, data–random, and random–random pairs, respectively. We generated a random sample that is 200 times the LAE sample size with the same geometry. A power-law form $w(\theta) = A\theta^{-\beta}$ was assumed for the angular correlation function. However, due to the limited size of the survey area, the observed angular correlation function is actually $w(\theta) = AC = A(\theta^{-\beta} - C)$, where AC is the integral constraint. By performing a Monte Carlo integration, we can first estimate $C$ (e.g., Roche et al. 1999) and then fit $A(\theta^{-\beta} - C)$ to the data. The clustering amplitude $A$ was thus obtained from the fitting by further fixing $\beta$ to 0.8 following the literature (e.g., Gualia et al. 2010; Matsuoka et al. 2011; Coupon et al. 2012). Note that we only used a selected range of $\theta$ ($50'' \lesssim \theta \lesssim 600''$) during the fitting, in order to avoid the influence of the one-halo term at small scales ($\theta < 50''$) and sampling noise at large scales. The best-fit values of $A$ and the integral constraint are $9.5 \pm 2.2$ arcsec$^{0.8}$ and 0.06, respectively. The angular two-point correlation function, along with the best-fit curve of our LAEs, is shown in Figure 15.

Corresponding to the power-law form of $w(\theta)$, the spatial correlation function has the form of $\xi(r) = (r/r_0)^{-3(\beta+1)}$. Assuming a Gaussian distribution of the LAE redshifts within our narrowband window, we obtained the real space correlation length according to Simon (2007), which is $3.66 \pm 0.47$ Mpc. Then we calculated the bias factor of LAEs by $b = \left(\frac{\xi_D}{\xi_{DM}}\right)^{1/3}$, where $\xi(r)$ and $\xi_{DM}(r)$ are the correlation function of LAEs and the underlying dark matter in the linear theory, respectively.
Here $r$ is chosen to be $8h^{-1}$ Mpc, following Ouchi et al. (2003) and Kusakabe et al. (2018). The resultant bias factor is $1.31 \pm 0.15$. Finally, the halo mass $M_h$ was obtained via the relation between bias factor and the peak height in the linear density field $\nu = \delta_c / \sigma(M_h, z)$ (Tinker et al. 2010), where $\delta_c = 1.686$ is the critical overdensity for dark matter collapse and $\sigma(M_h, z)$ is the rms fluctuation in a sphere that encloses mass $M_h$ on average at present time, extrapolated to redshift $z$ with the linear theory. The bias factor derived above corresponds to a mean dark matter halo mass of $\log(M_h/M_\odot) = 10.8^{+0.26}_{-0.42}$. Note that the errors reported here do not account for cosmic variance. Since our survey area (COSMOS and ECDF-S fields) is just $\sim 0.34$ deg$^2$, cosmic variance should be important, as discussed by Kusakabe et al. (2018). According to the scaling relation in Kusakabe et al. (2018), we estimated an uncertainty of $\sim 46\%$ owing to cosmic variance in the bias factor, resulting in a bias factor of $1.31 \pm 0.34$ and halo mass of $\log(M_h/M_\odot) = 10.8^{+0.56}_{-1.1}$. Most recently, based on a large sample (1937 LAEs) of $z \sim 2.2$ LAEs with NB387$_{tot}$ $\lesssim 25.5$ mag in four survey fields covering a total area of $\sim 1$ deg$^2$, Kusakabe et al. (2018) obtained a bias factor of $1.22^{+0.23}_{-0.25}$ and halo mass of $\log(M_h/M_\odot) = 10.6^{+0.5}_{-0.9}$. Accordingly, they predicted that in the local universe their LAEs would be typically hosted by dark matter halos with mass comparable to that of the Large Magellanic Cloud (LMC). The bias factor and halo mass based on our 446 LAEs are consistent with those of Kusakabe et al. (2018) within $1\sigma$, although the errors in our analysis are larger owing to the smaller survey area. Therefore, the dark matter halo hosting our LAEs may similarly evolve into an LMC-like halo at $z = 0$.

6. Summary

We have conducted deep narrowband surveys for the COSMOS and ECDF-S fields to search for LAEs at redshift $z = 2.25 \pm 0.03$ using our customized narrowband filter N393 at the Megacam/Magellan II telescope. Our observations reached a $5\sigma$ limiting magnitude in a 3$''$ diameter aperture of $\sim 26$ mag and a seeing FWHM of 0$''$.6. Using archival broad $U$- and $B$-band images as a measure of the underlying continuum, we selected 194 (including four AGNs) and 258 (including two AGNs) LAEs over the 602.05 arcmin$^2$ and 612.75 arcmin$^2$ survey areas on the COSMOS and ECDF-S fields, respectively. Our LAE sample provides reliable measurements of the Ly$\alpha$ luminosity function over the Ly$\alpha$ luminosity range of $10^{41.8}$–$10^{43.5}$ erg s$^{-1}$. Within this luminosity range, the Ly$\alpha$ luminosity functions of the COSMOS and ECDF-S fields are in a good agreement with each other. The overall shapes of our Ly$\alpha$ luminosity functions are consistent with that of Konno et al. (2016) and Sobral et al. (2017) based on larger-area (1.43 deg$^2$) Ly$\alpha$ surveys at similar redshifts. Thus, our Ly$\alpha$ luminosity functions lend further support to the steep faint-end slope.

The existing multiwavelength data from the rest-frame UV to the IR, especially the deep $Spitzer$/IRAC MIR data, allow us to explore the stellar populations and star formation properties of LAEs. The SEDS provides important constraints on the stellar mass estimates. For 29% of our LAEs that were detected by IRAC at 3.6 $\mu$m or 4.5 $\mu$m, their stellar masses are in the range of $8 < \log(M_*/M_\odot) < 11.5$. On the other hand, the SED fitting to the stacked SED of the IRAC-undetected LAEs indicates a stellar mass of $\log(M_*/M_\odot) = 7.97^{+0.05}_{-0.03}$ and dust extinction of $A_v = 0.12^{+0.25}_{-0.08}$ mag. Based on the measurement of the median stellar mass for the IRAC-undetected LAEs, we roughly estimate their mean number density as $\log(\Phi$/Mpc$^{-3}$sr$^{-1}) = -3.0$ at $\log(M_*/M_\odot) = 8$. Although it is a lower limit and much smaller than the extrapolation of the existing stellar mass functions, it serves as an important observational constraint at such a low-mass regime.

Rest-frame FUV luminosities calculated from the observed $B$-band flux densities were used to derive SFRs. The dust attenuations were estimated from the UV slope $\beta$, based on public $B$-, $V$-, $R$-, and $I$-band photometry. The dust-corrected SFRs of our LAEs cover a range of $1 M_\odot$ yr$^{-1} < $ SFR $< 100 M_\odot$ yr$^{-1}$, with six $Spitzer$/MIPS 24 $\mu$m or even Herschel FIR-detected LAEs having SFRs up to 2000 $M_\odot$ yr$^{-1}$. Although LAEs are heterogeneous populations that have stellar mass and SFR covering more than three orders of magnitude, i.e., $8 < \log(M_*/M_\odot) < 11.5, 1 M_\odot$ yr$^{-1} < $ SFR $< 2000 M_\odot$ yr$^{-1}$, they are mostly composed of low-mass galaxies and follow the SFMS relations and their extrapolations to the low-mass end. This indicates that the star formation in most LAEs is taking place in a steady mode.

The two-point correlation function analysis for our LAE sample yields a bias factor of $1.31 \pm 0.34$ and corresponding dark matter halo mass of $\log(M_h/M_\odot) = 10.8^{+0.56}_{-1.1}$, which is consistent with those of Kusakabe et al. (2018) based on a much larger sample and survey area.

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