Galaxy Evolution in the Environment of ABCG 209

C. P. Haines¹, A. Mercurio², P. Merluzzi¹, F. La Barbera¹, M. Massarotti¹, G. Busarello¹, and M. Girardi²

¹ Osservatorio Astronomico di Capodimonte, v. Moiarello 16, I-80131 Napoli, Italy
² Departamento di Astronomia, Università degli Studi di Trieste, v. Tiepolo 11, I-34100 Trieste, Italy

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Abstract. We examine the environmental effects on the photometric properties of galaxies for the rich galaxy cluster ABCG 209 at \(z = 0.209\). We use archive CFHT optical imaging of a 42 \(\times\) 28 arcmin\(^2\) field centred on the cluster to produce a galaxy sample complete to \(B = 25.0\) and \(R = 24.5\). Both the composite and red sequence galaxy luminosity functions are found to be dependent on the local galaxy surface density, their faint-end slopes becoming shallower with increasing density. We explain this as a combination of the morphology-density relation, and dwarf galaxies being cannibalised and/or disrupted by the cD galaxy and the ICM in the cluster core. The \(B - R\) colour of the red sequence itself appears 0.02 mag redder for the highest-density regions, indicative of their stellar populations being marginally (< 5%) older or (< 20%) more metal-rich. This may be due to the galaxies themselves forming earliest in the rarest overdensities marked by rich clusters, or their star-formation being suppressed earliest by the ICM.

Key words. Galaxies: clusters: individual: Abell 209; Galaxies: luminosity function; Galaxies: evolution

1. INTRODUCTION

The effect of local environment on the formation and evolution of galaxies is one of the most pressing issues in cosmology today, with evidence that environmental processes affect the mass distribution of galaxies, as well as their star-formation and morphological characteristics. Rich clusters provide a unique opportunity to study these environmental effects, providing large numbers of galaxies at the same redshift which have been exposed to a wide variety of environments. Numerous authors have studied the environmental effects of rich clusters on the luminosity functions, star-formation rates and morphologies of their constituent galaxies (e.g. López-Cruz et al. 1997, Balogh, Navarro & Morris 2000, Hogg et al. 2003, Treu et al. 2003).

The galaxy luminosity function (LF), which describes the number of galaxies per unit volume as a function of luminosity, is a powerful tool for examining galaxy formation and evolution, since it can be directly related to the galaxy mass function. The Press-Schechter prescription for the hierarchical assembly of galaxies predicts a simple analytical formula for the mass distribution of the form \(n(M)dM \propto M^n \exp(-M/M^*)\) (Press & Schechter 1974) which, despite not considering non-linear dynamical effects, reproduces well the results of N-body simulations of the growth of dark matter halos. This prescription was confirmed by the observation of Schechter (1978) that the galaxy luminosity function can be described by the Schechter function:

\[
\psi(L) dL = \psi^* \left(\frac{L}{L^*}\right)^\alpha \exp(-L/L^*) dL,
\]

where the shape of the LF is described by a characteristic cut-off luminosity \(L^*\), and \(\alpha\), the faint-end slope of the distribution. He also suggested that the shape of the galaxy LF is universal, and only the multiplicative constant \(\psi^*\) differs between clusters.

Numerous studies have since been made to determine the galaxy LF: some confirming the validity of the “universal luminosity function hypothesis” (e.g. Lugger 1980, Colless 1993, Trentham 1998); whereas others indicate that the LF is instead dependent on the environment of the galaxies, resulting in significant differences between the LFs from cluster to cluster and between cluster and field (e.g. López-Cruz et al. 1997, Valotto et al. 1997). More recent studies based on large surveys empirically suggest that the galaxy LF is indeed dependent on environment, with dynamically-evolved, rich clusters and clusters with central dominant galaxies having brighter characteristic luminosities and shallower faint-end slopes, than poorer clusters, those with substructure (López-Cruz et al. 1997, De Propris et al. 2003). In particular these differences can be explained through considering the composite LF as the sum of type-specific luminosity functions (TSLFs), each with its universal shape for a specific type of galaxies (e.g. elliptical, spiral, dwarf). The shape of the
composite LF then can vary from cluster to cluster, and from cluster to field, according to the mixture of different galaxy types in each environment resulting from the morphology-density relation (Dressler et al. 1987; Binggeli et al. 1988).

The galaxies most synonymous with the cluster environment are the bulge-dominated, passively-evolving galaxies which make up the cluster red sequence. Studies of low-redshift clusters (e.g. Bower, Lucey & Ellis 1992) indicate that, irrespective of the richness or morphology of the cluster, all clusters have red sequences, whose k-corrected slopes, scatters and colours are indistinguishable. Other studies find similar precise regularities between other physical properties of the early-type galaxies (surface-brightness, mass-to-light ratio, radius, velocity distribution, metallicity) resulting in the Faber-Jackson (Faber & Jackson 1976) and Kormendy (1977) relations and the fundamental plane (Djorgovski & Davis 1987; Dressler et al. 1987). These all indicate that the early-type galaxies which make up the red sequences form a homogeneous population, not only within each cluster, but from cluster to cluster, and also that red sequences are universal and homogeneous features of galaxy clusters, at least at $z<0.2$.

The photometric evolution of the cluster red sequence with redshift has been studied by a number of authors (e.g. Aragón-Salamanca et al. 1993; Ellis et al. 1997; Stanford et al. 1998; Kodama et al. 1998) for clusters out to $z \approx 1.2$ indicating that red sequence remains a universal feature of clusters; that the stellar populations of its constituent early-type galaxies are formed in a single, short burst at an early epoch ($z_f \approx 2$); and that the galaxy colours have evolved passively ever since. This is confirmed by the spectra of red-sequence galaxies which in nearby clusters are best fit by simple stellar populations of ages 9–12 Gyr, resulting in their having characteristically strong spectral breaks at 4000 Å, and correspondingly red $U-V$ colours.

Cosmological models of structure formation indicate that the densest regions of the universe corresponding to the rarest overdensities in the primordial density field will have collapsed earliest, and will contain the most massive objects, i.e. rich galaxy clusters. Detailed cosmological simulations which follow the formation and evolution of galaxies (e.g. Kauffmann 1998; Blanton et al. 2003) predict that galaxies in these high-density regions are older and more luminous than those in typical density (i.e. field) regions. Having initially ($z \sim 5$) been the most likely place for the formation of stars and galaxies, the high-density environment of rich cluster cores is later ($z \sim 1-2$) filled with shock-heated virialised gas that does not easily cool and collapse (Blanton et al. 1999), inhibiting both the formation of stars and galaxies (Blanton et al. 2000), which instead occurs most efficiently in increasingly less massive dark matter halos. These models are able to successfully predict the observed cluster-centric star-formation and colour gradients, and the morphology-density relation of $z<0.5$ clusters (Balogh et al. 2000; Diaferio et al. 2001; Springel et al. 2001; Okamoto & Nagashima 2003), although it is not clear whether they predict trends with density of colour or star-formation for galaxies of a fixed morphology and luminosity. They show that these gradients in galaxy properties naturally arise in hierarchical models, because mixing is incomplete during cluster assembly, and the positions of galaxies within the clusters are correlated with the epoch at which they were accreted.

To examine the effect of environment on galaxy properties, in particular the galaxy luminosity function, and the cluster red sequence, we have performed a photometric study of the galaxy cluster A209 at $z = 0.21$ (Kristian, Sandage & Westphal 1978; Wilkinson & Oke 1978; Ebeling et al. 1996). The photometric properties of the cluster galaxies to be followed out to radii of $3-4h_{70}^{-1}$ Mpc. A209 is a rich (richness class R = 3; Abell et al. 1989), X-ray luminous ($L_X(0.1-2.4\text{keV}) \approx 2.7 \times 10^{45}h_{70}^{-2}\text{erg s}^{-1}$, Ebeling et al. 1996) $T_X \sim 10\text{keV}$, Rizza et al. 1998), and massive cluster (Mercurio et al. 2003b) but see also Dahle et al. 2002). The cluster was initially chosen for its richness, allowing its internal velocity field and dynamical properties to be studied in great detail, and also for its known substructure, allowing the effect of cluster dynamics and evolution on the properties of its member galaxies to be examined. This substructure is manifested by an elongation and asymmetry in the X-ray emission with two main clumps (Rizza et al. 1998), but no strong cooling flow is detected. Moreover, the young dynamical state is indicated by the possible presence of a radio halo (Giovannini, Tordi & Feretti 1999), which has been suggested to be the result of a recent cluster merger, through the acceleration of relativistic particles by the merger shocks (Feretti et al. 2000).

The internal dynamics of the cluster were studied by Mercurio et al. (2003b) through a spectroscopic survey of 112 cluster members. A high value of the line-of-sight velocity dispersion was found, with $\sigma_v = 1394^{+88}_{-95}\text{km s}^{-1}$. Assuming dynamic equilibrium, this value of $\sigma_v$ leads to a virial radius of $R_{200} \sim 2.5h_{70}^{-1}\text{Mpc}$, and a virial mass of $M(R < R_{200}) = 2.3-3.1 \times 10^{15}h_{70}^{-1}\text{M}_\odot$.

Evidence in favour of the cluster undergoing a dynamical evolution is found in the form of a velocity gradient acting along a SE-NW axis, which is the same preferential direction found from the elongation in the spatial distribution of galaxies and X-ray flux, as well as that of the cD galaxy. There is also significant deviation of the velocity distribution from a Gaussian, with evidence for two secondary clumps at $z = 0.199$ and $z = 0.215$, which appear spatially segregated from the main cluster. These all indicate that A209 is undergoing strong dynamic evolution with the merging of two or more sub-clumps along the SE-NW direction. This dynamical situation is confirmed by the weak lensing analysis of Dahle et al. (2002), which shows the cluster to be highly elongated in the N-S direction, and two significant peaks, the largest coincident with the cluster centre and cD galaxy, and the second 6 arcmin to the north.

The cluster was studied previously using optical data covering a 78 arcmin$^2$ (160 arcmin$^2$ in V) region, reaching
$B = 22.8$, $V = 22.5$ and $R = 22.0$, and galaxy luminosity functions determined for each passband (Mercurio et al. 2003b).

The photometric data are presented in Section 2. As this cluster has been found to be significantly elongated along the SE-NW direction, we examine the effect of the cluster environment by measuring galaxy properties as a function of local surface density rather than cluster-centric radius. We describe the method for determining the cluster environment in Sect. 3. The ability to successfully subtract the background field population is vital to study the global properties of cluster galaxies from photometric data alone, and we describe the approach to this problem in Sect. 4. The composite galaxy LF is presented in Sect. 5, and the properties of the red sequence galaxies described in Sect. 6. The effects of environment on the blue galaxy fraction and mean galaxy colours are presented in Sects. 7 and 8. Sect. 9 is dedicated to the summary and discussion of the results. In this work we assume $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_m = 0.3$, and $\Omega_\Lambda = 0.7$. In this cosmology, the lookback time to the cluster A 209 at $z = 0.209$ is 2.5 Gyr.

2. THE DATA

The data were obtained from the Canada-France-Hawaii telescope (CFHT) science archive (PI. J.-P. Kneib), comprising wide-field $B$- and $R$-band imaging centred on the cluster A 209. The observations were made on 14–16 November 1999, using the CFHT12K mosaic camera, an instrument made up of 12 4096×2048 CCDs, set at 512×256. The data were taken in photometric conditions. The distortion produced by the camera optics is modelled with 4 contiguous pixels 1″ wide, resulting in a total field of view of $42 \times 28$ arcmin$^2$, corresponding to $8.6 \times 5.7 h_7^2 \text{ Mpc}^2$ at the cluster redshift. The total exposure times for both $B$- and $R$-band images are 7200s, made up of eight 900s $B$-band and twelve 600s $R$-band exposures, jittered to cover the gaps between the CCDs.

Standard procedures were used to bias-subtract the images, using bias exposures and the overscan regions of each CCD. Saturated pixels and bleed trails from bright stars are identified and interpolated across. The images were then flat-fielded using a superflat made up of science images taken using the same camera/filter setup of cluster A 209, as well as those of the clusters A 68, A 383, A 963, Cl 0818 and Cl 0819 which were also observed as part of the same observing program. For each image, the sky is subtracted by fitting a quadratic surface to each CCD. The sky is then modelled using a 256 × 256 pixel median filter, rejecting all pixels $>3\sigma$ from the median (i.e. galaxies).

Cosmic rays are removed by comparison of each image with a registered reference image (taken to be the previous exposure). After masking off those pixels $3\sigma$ above the median in the reference image (taken to be sources) each pixel which has a value $>3\sigma$ higher than its value in the reference image, is flagged as a cosmic ray and interpolated across. The individual images are corrected for airmass using the prescribed values from the CFHT website of the cluster redshift. The total exposure times for both $B$- and $R$-band images are 7 200s, made up of eight 900s $B$-band exposures, jittered to cover the gaps between the CCDs, there is some overlap between the coadded images of adjacent CCDs. This is used to create linear transforms allowing 12 CCDs to be “stitched” together to form an interim coadded image. This interim image is then used as a reference to which each individual exposure is registered. The registered exposures are then coadded after masking out the gaps between CCDs and bad columns, using $3\sigma$ clipping. The distortion produced by the camera optics is modelled and removed as a quartic-polynomial fit to the positions of GSC2 sources in a reference tangential plane astrometry.

The photometric calibration was performed into the Johnson–Kron–Cousins photometric system using observations of $\sim 300$ secondary standard stars ($14 < R < 17$) in fields 6 and 7 of Galadi-Enríquez, Trullols & Jordi (2000). The fields also contain equatorial standard stars of Landolt (1992) tying the photometric calibration to the Landolt standards, while allowing the uncertainty of the zeropoint and colour-terms to be reduced and measured in a statistical manner. The median photometric uncertainty for each standard star was $\Delta(B) = 0.033$, and $\Delta(R) = 0.021$. The zero-points and colour terms were fitted using a weighted least-squares procedure, and are shown in Table 1 along with the observed FWHMs of each image. Object detection was performed using SExtractor in two-image mode (Bertin & Arnouts 1996) for sources with 4 contiguous pixels $1\sigma$ over the background level in the $R$-band image. The total $B$ and $R$ magnitudes were taken to be the Kron magnitude, for which we used an adaptive elliptical aperture with equivalent diameter $a r_K$, where $r_K$ is the Kron radius, and $a$ is fixed at a constant value of 2.5. $B - R$ colours were determined using fixed apertures of $5\text{ arcsec}$ diameter (corresponding to $\sim 17\text{ kpc}$ at $z = 0.209$), after correcting for the differing seeing of the $R$- and $B$-band images. The measured magnitudes were corrected for galactic extinction following Schlegel, Finkbeiner & Davis (1998) measured as $E(B-V) = 0.019$, giving $A(B) = 0.083$ and $A(R) = 0.051$. The uncertainties in the magnitudes were obtained by adding in quadrature both the uncertainties estimated by SExtractor and the uncertainties of the photometric calibrations.

| Band FWHM | Colour | Zeropoint | Colour Term |
|-----------|--------|-----------|-------------|
| $B$       | 1.02  | $B - R$   | $25.720 \pm 0.008$ | $-0.0180 \pm 0.005$ |
| $R$       | 0.73  | $B - R$   | $25.983 \pm 0.005$ | $0.0002 \pm 0.004$ |

Table 1. Photometric parameters of optical data.
Fig. 1. Completeness magnitudes of the $B$- and $R$-band images, as estimated by comparing the magnitudes in the fixed aperture ($m_{ap}$) and in the detection cell ($m_{cell}$). The horizontal solid lines represent the completeness limits, the vertical dot-dashed lines mark the limits in the detection cell, and the dashed lines are the linear relations between $m_{ap}$ and $m_{cell}$.

The completeness magnitudes were derived following the method of Garilli, Maccagni & Andreon (1999), as shown in Fig. 1 which compares the magnitudes in the fixed aperture ($m_{ap}$) and in the detection cell ($m_{cell}$) which in our case is an aperture of area 4 pixels. The magnitude limits at which galaxies are lost due to being fainter than the threshold in the detection cell are determined, and are indicated by the vertical dot-dashed lines. There is a correspondence between $m_{cell}$ and $m_{ap}$ as shown by the dashed line, which has a certain scatter that depends essentially on the galaxy profile and the photometric errors. To minimise biases due to low-surface brightness galaxies, the completeness magnitude limits are chosen to consider this dispersion, and are indicated by the horizontal solid lines at $B = 25.0$ and $R = 24.5$. For the analyses of the cluster red sequence, we consider a magnitude limit of $R = 23.0$, in order that we remain complete for galaxies with $B - R \sim 2.0$.

2.1. Star - Galaxy Separation

Star-galaxy separation is performed using the SExtractor stellarity index, with stars defined as sources with stellari-
ties $\geq 0.98$. By examination of the distributions of sources classified as stars and galaxies in the magnitude-FWHM plane, and the number-magnitude distribution of sources classified as stars, we believe the classification to be efficient to $R \sim 22$ and $B \sim 23$, where stars constitute 12% of all sources.

Figure 2 (top) shows the number-magnitude distribution of sources classified as stars by SExtractor. For $19 < R < 22$ the distribution behaves as a power-law as would be expected (see Groenewegen et al. 2002). At brighter magnitudes, stars become saturated, while at fainter magnitudes, the classifier begins to misclassify stellar sources as galaxies. By extrapolating the power-law to fainter magnitudes, as indicated by the solid diagonal line, we estimate the level of contamination by stars in the range $22 < R < 23$ to be $\approx 200$ over the whole field (0.18 stars arcmin$^{-2}$), or $\sim 5 \%$ of all sources. However, since the contamination from faint stars should affect those regions used to define the field galaxy population at the same level as for the cluster regions, when we correct for field galaxy contamination, the contamination due to faint stars should automatically cancel out also.

Figure 2 (bottom) shows the $B - R$ colour distribution of stars in the range $19 < R < 22$. The y-axis is normalised to represent the expected level of contamination by stars in the range $22 < R < 23$ to be $\approx 200$ over the whole field, i.e. 200 in total, assuming the colour distribution remains constant. The distribution is clearly bimodal with two sharp peaks at $B - R \sim 1.0$ and $B - R \sim 2.7$ indicating...
3. Defining the Cluster Environment

To study the effect of the cluster environment on galaxies in the vicinity of A 209, the local surface density of galaxies, $\Sigma$, is determined across the CFHT images. This is achieved using an adaptive kernel estimator (Pisani 1993, 1996), in which each galaxy is represented by an exponential kernel, $K(r) \propto \exp(-r/r_0)$, whose width, $r_0$ is proportional to $\Sigma^{-1/2}$, thus ensuring greater resolution where it is needed in the high-density regions, and more smoothing in the low-density regions where the signal-to-noise levels are much lower. For this study, the surface number density of $R < 23.0$ galaxies is considered, the magnitude limit to which cluster red sequence galaxies can be detected in both passbands. The local density for each galaxy is initially determined using an exponential kernel whose width is fixed to 60 arcsec, and then iteratively recalculated using adaptive kernels, before corrected for field contamination. The resultant surface number density map of the A 209 field is shown in Fig. 3. The dashed contour corresponds to the density of field galaxies, while the thick contours correspond to 2, 5 and 10 cluster galaxies arcmin$^{-2}$, the densities used to separate the three cluster environments described below.

The spatial distribution shows the complex structure of this cluster, characterised by the clear elongation in the SE-NW direction (see Mercurio et al. 2003a), indicative of the cluster having gone through a recent merger event. There are also present three other subclumps, the first one about 10 arcmin south along the cluster elongation, the second at about 18 arcmin to the north-east, and the last one, the smallest, at about 18 arcmin to the southwest. The colour information on galaxies in these peaks confirm that these could be groups/clusters at the same redshift as A 209. Given the complexity
of the structure of A 209, it is important that to study the effect of environment on galaxy properties, we measure them as a function of local galaxy number surface density rather than cluster-centric radius as is usual in these type of studies.

For the following analyses on the effect of the cluster environment on its constituent galaxy population we define three regions selected according to the local surface number density. Firstly we consider a high-density region with \( \Sigma > 10 \) gals arcmin\(^{-2} \), which corresponds to the cluster core out to a radius of \( \approx 500 \) kpc, and covers 16.0 arcmin\(^2 \). Next we consider intermediate- (5 < \( \Sigma < 10 \) gals arcmin\(^{-2} \)) and low-density (2 < \( \Sigma < 5 \) gals arcmin\(^{-2} \)) regions which probe the cluster periphery with median galaxy cluster-centric radii of 1.3 and 2.2 Mpc, and cover 68.0 and 189.6 arcmin\(^2 \) respectively. It should be stated that in each case we are studying the cluster galaxy population and not that of the field, and the low-density environment represents an overdense region.

### 4. Statistical Field Galaxy Subtraction

To accurately measure the properties of the cluster population as a function of environment requires the foreground / background contamination to be estimated efficiently and corrected. Given the lack of spectroscopic information, we estimate the field galaxy contamination as a function of magnitude and colour (see also Kodama & Bower 2001).

The sample of field galaxies is taken from two regions within the CFHT12K field indicated in Fig. 3 by the shaded boxes. These areas were identified as regions where the local galaxy surface density reached a stable minimum level over a wide area indicative of the field. They also have galaxy number counts within 1\( \sigma \) of the ESO-Sculptor survey of Arnouts et al. (1997) which covers an area of 0.24 \( \times \) 1.52 deg\(^2 \), and is complete to \( B = 24.5 \) and \( R = 23.5 \). The two “field” regions in the A 209 field cover in total 160.9 arcmin\(^2 \), and contain 965 galaxies to \( R = 23.0 \), resulting in a number surface density of 6.0 gals.arcmin\(^{-2} \), as indicated in Fig. 4 by the dashed contour.

A two-dimensional distribution histogram of these field galaxies is built with bins of width 0.25 mag in \( B - R \) colour and 0.5 mag in \( R \) magnitude. Similar histograms are the constructed for each of the three cluster regions, which also obviously include a field galaxy contamination. The field histogram is normalised to match the area within each cluster region, and for each bin \((i,j)\) the number of field galaxies \( N_{i,j}^{field} \) and the cluster plus field \( N_{i,j}^{cluster+field} \) are counted. The former can be larger than the latter for low-density bins due to low number statistics, in which case the excess number of field galaxies are redistributed to neighbouring bins with equal weight until \( N_{i,j}^{field} < N_{i,j}^{cluster+field} \) is satisfied for all bins. For each galaxy in the cluster region the probability that it belongs to the field is then defined as:

\[
P(field) = \frac{N_{i,j}^{field}}{N_{i,j}^{cluster+field}},
\]

where the numbers are taken from the bin that the galaxy belongs to. For each cluster region, 100 Monte-Carlo simulations of the cluster population are realised and averaged.

The \( B - R/R \) C-M diagrams for Monte-Carlo realisations of the cluster galaxy population for each of the three cluster regions corresponding to high-, intermediate-, and low-density environments are shown in Fig. 4 along with that for the field region used for the statistical field subtraction. The different distributions of the cluster and field populations are obvious, with the red sequence prominent in both high- and intermediate-density regions.

### 5. The Galaxy Luminosity Function

In order to measure the cluster LF in each band we used all the galaxy photometric data up to the completeness magnitudes and removed the interlopers by statistically
subtracting the background contamination, as determined from the two field regions. The errors on the cluster LFs are computed by adding in quadrature the Poisson fluctuations for the galaxy counts in both the cluster and field regions, and fluctuations due to photometric errors on Kron magnitudes.

We compute the cluster LFs for both $B$ and $R$ bands for galaxies within one virial radius, and examine the effect of the cluster environment by determining the LFs for each of the three cluster regions corresponding to high-, intermediate- and low-density environments. For each cluster LF, we fit the observed galaxy counts with a single Schechter function. Absolute magnitudes are determined using the k-corrections for early-type galaxies from Poggianti (1997). All the fit parameters and associated $\chi^2$ statistics are listed in Table 2.

5.1. Galaxies within the Virial Radius

Figure 5 shows the LFs in the $B$ and $R$ bands for galaxies within one virial radius ($2.5h^{-1}_{70}$ Mpc) of the cluster centre. The solid curves show the best-fitting single Schechter functions, obtained by weighted parametric fits to the statistically background-subtracted galaxy counts. According to the $\chi^2$ statistic, the global distributions of the data are well described by single Schechter functions, although...
Fig. 8. The R-band LFs of galaxies in the three cluster regions corresponding to high-, intermediate- and low-density environments.

Fig. 9. Confidence limits for the best-fitting Schechter parameters $\alpha$ and $R^*$ for the three cluster regions. Contours as for Fig. 7.

Table 2. Fits to the LFs for cluster galaxies. Errors on the $M^*$ and $\alpha$ parameters are indicated by the confidence contours shown in Figures 5, 7 and 9.

In Mercurio et al. (2003b) we derived the LFs for the central field of $9.2' \times 8.6'$ ($1.9 \times 1.8 h_{70}^{-2}$ Mpc$^2$) by using EMMI–NTT images, complete to $B = 22.8$ and $R = 22.0$. In this previous study we subtracted statistically the field contamination using background counts in B- and R-bands from the ESO-Sculptor Survey (Arnouts et al. 1997; de Lapparent et al. 2003). The parameters of the best-fitting Schechter functions were: $B^* = 20.06$, $\alpha_B = -1.26$, and $R^* = 17.78$, $\alpha_R = -1.20$, which are fully consistent with those derived here.

5.2. The effect of environment

To examine the effect of environment on the galaxy LF, we have determined the B- and R-band LFs for galaxies in three regions selected according to their local density. Figures 6 and 8 show respectively the B- and R-band LFs in the three different cluster regions, corresponding to high-, intermediate-, and low-density environments. Each LF is modelled through use of a weighted parametric fit to a single Schechter function, the results of which are presented in Table 2.

As for the region within one virial radius, the single Schechter function gives a good representation of the global distribution of the data for each cluster environment in both B- and R-bands. In both high- and low-density regions, no dip is apparent at $R = 20–21$, although the observed counts are marginally below that predicted from the Schechter function. Only in the intermediate-density region is a significant dip apparent, where a deficit of $R = 20.0–20.5$ galaxies significant at the 2$\sigma$ level is observed with respect to the fitted Schechter function.

Figures 4 and 10 show the confidence contours for the best fitting Schechter functions for $\alpha$ and $B^*$, and $\alpha$ and $R^*$ respectively, for each of the three cluster regions, allowing the trends with density to be followed. In both B and R bands, the faint-end slope becomes significantly steeper from high- to low-density environments, the values of $\alpha$ determined for the high- and low-density regions being inconsistent at more than the 3$\sigma$ confidence level.
6. Properties of the Red Sequence Galaxies

We determined the colour-magnitude (CM) relation of galaxies in the cluster A 209 by averaging over 100 Monte-Carlo realisations of the cluster population, and fitting the resultant photometric data of the ~ 480 $R < 21$ galaxies within one virial radius with the biweight algorithm of Beers et al. (1990) obtaining

\[(B - R)_{CM} = 3.867 \pm 0.006 - 0.0815 \pm 0.0098 \times R. \tag{3}\]

Here the errors quoted consider the uncertainty due to background subtraction, photometric errors, and uncertainty from the fitting itself as measured using the scale value of the biweight algorithm. The $B - R$ colour dispersion around the red sequence is measured as a function of magnitude, $\sigma(R)$, for galaxies in each magnitude bin over the range $18 < R < 23$. It is found to be consistent with being due to an intrinsic colour dispersion, $\sigma_{int}$, and the photometric error, $\sigma_{B-R}^2(R)$ added in quadrature,

$$\sigma(R)^2 = \sigma_{int}^2 + \sigma_{B-R}^2(R). \tag{4}$$

The intrinsic dispersion around the red sequence is found to be $\sigma_{int} = 0.10$ mag, which is much higher than the dispersion level of 0.05 mag found for the Coma and Virgo clusters (Bower, Lucey & Ellis 1992), and which is often quoted as being typical for low redshift rich clusters. However, in a similar study of the $B - R/R$ CM-relation for $11.07 < z < 0.16$ clusters Pimbblet et al. (2002) obtain typical dispersion levels of 0.06–0.08, and observe three clusters with dispersion levels higher than ours.

Using this equation, we then defined those galaxies lying within the region between the curves:

\[(B - R)_\pm = (B - R)_{CM} \pm \sqrt{\sigma_{int}^2 + \sigma_{B-R}^2} \tag{5}\]

as being red sequence galaxies.

As for the composite luminosity function, we determine the $R$-band luminosity function of red sequence galaxies within one virial radius of the cluster centre, as shown in Figure 11.

6.1. The effect of environment on the C-M relation

We also determine the C-M relation in the high- and intermediate-density regions separately, to see if there is any environmental effect on the relation. By fixing the slope at -0.0815, we find the red sequence to be $0.022 \pm 0.014$ mag redder in the high-density region than for the intermediate-density region. The effect of environment on the red sequence slope was also examined by leaving the slope as a free parameter, but no significant change was observed. It was not possible to extend this analysis to the low-density region, as the red sequence was poorly constrained due to a much larger contamination by outliers.

The $R$-band luminosity functions of red sequence galaxies (as selected according to Eq. 5) in each of the three cluster environments is shown in Figure 11 and the best fitting parameters shown in Table 8. The solid curve shows the best-fitting Schechter function found through a maximum likelihood analysis whose parameters $\alpha$ and $R^*$ are indicated in the top-left of each plot. The errors for each bin are determined as the uncertainty from the field galaxy subtraction and the Poisson noise due to galaxy counts in the cluster and field regions, all added in quadrature.

For the cluster red sequence we consider a magnitude limit of $R = 23.0$. At this magnitude, red sequence galaxies have $B - R \sim 2.0$, and so are at the completeness limit of the $B$-band image, and have typical uncertainties...
Fig. 11. The $R$-band LFs of red sequence galaxies in the three cluster regions corresponding to high-, intermediate- and low-density environments. The solid curve indicates the best-fitting Schechter function whose parameters are indicated in the top-left of each plot.

| Region          | $R^*$ | $M^*$ | $\alpha$ | $\chi^2$ |
|-----------------|-------|-------|----------|----------|
| $r < R_{vir}$   | 17.94 | -22.22 | -1.08    | 1.61     |
| $\Sigma > 10$  | 18.04 | -22.30 | -0.97    | 0.95     |
| $5 < \Sigma < 10$ | 17.94 | -22.20 | -1.00    | 0.45     |
| $2 < \Sigma < 5$ | 17.90 | -22.24 | -1.15    | 0.90     |

Table 3. Fits to the red sequence galaxy LFs. Errors on the $R^*$ and $\alpha$ parameters are indicated by the confidence contours shown in Figs. 10 and 12.

of $\Delta(R) \sim 0.06$ and $\Delta(B-R) \sim 0.11$. As discussed earlier, the expected contamination of stars is minimal due to their colour-distribution, and for the three cluster regions corresponding to high-, intermediate-, and low-density environments, should be at the level of 0.1, 0.3 and 0.8 stars respectively.

Figure 12 shows the confidence contours for the best-fitting Schechter parameters $\alpha$ and $R^*$ for each of the three cluster regions, allowing the trends with density to be followed. As for the overall galaxy luminosity function, the $R$-band luminosity function of red sequence galaxies has a steeper faint-end slope, $\alpha$, in the low-density regions than for their high-density counterparts, although the effect here is smaller, and significant only at the 1.7$\sigma$ level. Also in each of the three cluster environments, the faint-end slope for the overall galaxy luminosity function is steeper than that for the luminosity function of red sequence galaxies only. This is due to the red sequence galaxies dominating at bright magnitudes, while at faint magnitudes they constitute only $\sim 25\%$ of the cluster population.

7. Blue Galaxy Fraction

One of the classic observations of the study of galaxy evolution is the Butcher-Oemler [1984] effect in which the fraction of blue galaxies in clusters is observed to increase with redshift. Here instead we consider the effect of environment on the fraction of blue galaxies. We define the blue galaxy fraction as the fraction of $R < 20$ ($\sim M^* + 2$) galaxies with rest-frame $B - V$ colours at least 0.2 mag bluer than that of the C-M relation, as for the original studies of Butcher & Oemler [1984]. We estimate the corresponding change in $B - R$ colour at the cluster redshift by firstly considering two model galaxies at $z = 0$ (Bruzual & Charlot 1993), one chosen to be a typical red-sequence galaxy (10 Gyr old, $\tau = 0.1$ Gyr, $Z = 0.02$), and the second reduced in age until its $B - V$ colour becomes 0.2 magnitude bluer. After redshifting both galaxies to the cluster redshift, the difference in their observed $B - R$ colour is found to be 0.447 mag. Hence we consider the blue galaxy fraction to be the fraction of $R < 20$ galaxies having $B - R < 3.420 - 0.0815 \times R$. Figure 13 shows the resulting blue galaxy fractions in the high-, intermediate-
Fig. 14. The mean galaxy colour of the cluster galaxy population as a function of spatial position (see text).

8. Galaxy colours

To gain some further insight into the effect of cluster environment and also the particular dynamical state of A 209, we plot in Figure 14 the mean $B - R$ colour of $R < 21$ cluster galaxies as a function of spatial position. This is determined as for the surface density map of Fig. 3 through the adaptive kernel approach (Pisani 1993, 1996), in which each galaxy is weighted according to the probability that it is a cluster member, $1 - P(f)$, so that for a particular point, $x$, the local mean galaxy colour is given by:

$$\langle B - R \rangle_x = \frac{\sum_{i=1}^{N}(B - R)_i^{CM} \cdot (1 - P(f)_i) \cdot K(x - x_i; r_i)}{\sum_{i=1}^{N}(1 - P(f)_i) \cdot K(x - x_i; r_i)}$$  \hspace{1cm} (6)

where $x_i$, $P(f)_i$, and $r_i$ are the position, probability of being a field galaxy, and kernel width respectively of galaxy $i$ out of $N$. And $(B - R)_i^{CM}$ is the $B - R$ colour for each galaxy after accounting for the luminosity-dependent effect of the slope of the CM-relation through

$$(B - R)_i^{CM} = (B - R)_0 + 0.0815 \times (R_i - 19).$$  \hspace{1cm} (7)

The resultant mean galaxy colour map $\langle B - R \rangle(x)$ is shown by the coloured contours, with the red/orange contours indicating regions which have redder cluster galaxies on average, and blue/purple contours indicating regions which have more blue cluster galaxies. To see how the colour of these cluster galaxies are related to their environment, the contours are overlaid upon the same contour map of the surface number density of $R < 23.0$ galaxies as shown in Fig. 3.

What is most important is that only the cluster galaxy population is being examined, and so the fact that field galaxies are bluer on average than cluster galaxies should not result in a density-dependent colour gradient, as would be the case if all galaxies were considered. Instead, any surface density-dependent colour gradient should be purely the result of galaxies in the low-density environments on the cluster periphery having differing colours on average to those in high-density environments. Secondly, as it is the mean $B - R$ colour of $R < 21$ galaxies that is being measured, it is the effect of the cluster environment on only the luminous cluster galaxies ($L \geq 0.1L^\ast$) that is being examined.

A clear overall density-dependence on galaxy colour is apparent, with galaxies in the high-density regions having $\mu(B - R) \sim 2.21 - 2.30$, while galaxies in the low-density regions have $\mu(B - R) \sim 2.14 - 2.18$. This we take to be the manifestation of the same effect observed with the blue galaxy fraction, with higher blue galaxy fractions on the cluster peripheries, thus reducing the mean $B - R$ colour in those regions.

Substructure in the mean $B - R$ galaxy colours is apparent, and appears related to the dynamical state of the system, being aligned with the direction of elongation in the galaxy number surface density. The reddest mean $B - R$ galaxy colours are observed at the very centre of the cluster, coincident with the cD galaxy and a concentration of the brightest $R < 19$ galaxies, as would be expected. There also appear regions of red galaxies on either side of the cluster core aligned with the overall elongation of the cluster. As the overall galaxy surface density is greater in the NW direction from the cluster core, we would suggest that this is where the merging clump is found, some 4–5 arcmin from the centre of A 209, corresponding to ~ 1 Mpc at $z = 0.209$.

In contrast, perpendicular to the axis of elongation appear regions close to the cluster centre containing bluer than average galaxies. The concentration to the east appears centred on a bright face-on spiral ($R = 17.71$, $B - R = 1.47$), which has been spectroscopically confirmed as a cluster member (Mercurio et al. 2003a).
9. DISCUSSION

We have examined the effect of cluster environment, as measured in terms of the local surface density of \( R < 23.0 \) galaxies, on the global properties of the cluster galaxies, through their luminosity functions, colour-magnitude relations, and average colours. For this study we have considered three cluster environments, a high-density region sampling the cluster core, and intermediate- and low-density regions which sample the cluster periphery.

9.1. The Galaxy Luminosity Function

The LFs for galaxies within the virialised region are found to be well described by single Schechter functions to \( M \) \( R \), \( M_R \sim -16 \), although there is an indication of a dip at \( R = 20-20.5 \) \( (M_R = -20) \). Dips in the LF at such absolute magnitudes appear common for low-redshift clusters (see Mercurio et al. 2003). Deficit in the LF is found to be stronger for richer, early-type-dominated clusters (Yagi et al. 2002).

The faint-end slope, \( \alpha \), shows a strong dependence on environment, becoming steeper at \( > 3\sigma \) significance level from high- to low-density environments. We explain this trend as the combination of two related effects: a manifestation of the morphology-density relation whereby the fraction of early-type galaxies which have shallow faint-end slopes increases with density, and the expense of late-type galaxies which have steep faint-end slopes; and a luminosity-segregation due to dwarf galaxies being cannibalised by the cD galaxy and the ICM in the cluster core.

To separate the two effects, we consider the TSLF of galaxies belonging to the cluster red sequence, as these are predominantly early-type galaxies, and so any trends with environment should be independent of the morphology-density relation. Some luminosity-segregation is observed, with a reduction in the fraction of dwarf galaxies in the high-density regions, as manifested by their shallower TSLF faint-end slopes. This effect is smaller than that for the overall LF, being significant only at the 1.7\( \sigma \) level, indicating that both luminosity-segregation and the morphology-density relation drive the observed trends in the overall LF. Luminosity-segregation is predicted by simulations for early-type galaxies in clusters, with bright early-type galaxies much more concentrated than their faint counterparts which follow the distribution of the dark matter mass profile (Springel et al. 2001).

In a study of 45 low-redshift \( (0.04 < z < 0.18) \) clusters, López-Cruz et al. 1997 find that for the seven that are rich, dynamically-evolved clusters, characterised by the presence of a cD galaxy, their composite LFs are all well described by single Schechter functions with shallow faint-ends \( (\alpha \approx 1.0) \). In contrast other clusters, often poorer, but in particular those not containing a cD galaxy, require two Schechter functions to fit their LFs, including a steep faint-end slope to model the dwarf population (see also Parolin, Molinari & Chincarini 2003). We thus indicate that the shallow faint-end slope observed in the high-density region of A 209 is related to the presence of the central dominant galaxy. cD galaxies are regarded as physically different to elliptical galaxies, with a different formation history, and are the product of dynamic processes which take place during the formation of their host cluster. They are thought to be built up through galactic cannibalism, or the accumulation of tidal debris. López-Cruz et al. 1997 propose that the flatness of the faint-end slope in clusters containing cD galaxies results from the disruption of a large fraction of dwarf galaxies during the early stages of cluster evolution, the stars and gas of which are cannibalised by the cD galaxy, and the remainder redistributed into the intracluster medium.

9.2. Environmental Effects on the Red Sequence

As well as having an effect on the TSLF of red sequence galaxies, the cluster environment could have an affect on the colour or slope of the red sequence itself, through the mean ages or metallicities of the galaxies. To examine this possibility the red sequence was fitted for the high- and intermediate-density regions independently. The red sequence was found to be 0.222 ± 0.014 mag redder in the high-density region than for the intermediate-density region by fixing the slope. In contrast no correlation between the slope of the red sequence and environment was observed. A similar effect is observed for bulge-dominated galaxies taken from the Sloan Digital Sky Survey (SDSS) (Hogg et al. 2003), in which the modal 0.1\( |g - r| \) residual colour to the best-fitting C-M relation is 0.01–0.02 mag redder in the highest-density environments (corresponding to cluster cores) than in their low-density counterparts. In a study of 11 X-ray luminous clusters at \( 0.07 < z < 0.16 \) Pimbblet et al. 2002 examine the red sequence as a function of cluster-centric radius and local galaxy density, and observe that the relation becomes progressively bluer as cluster-centric radius is increased out to 3Mpc, and as the local surface density is decreased at a rate of \( d(B-R)/d\log_10(\Sigma) = -0.08 \pm 0.01 \). In a study of the cluster A 2390 at \( z = 0.23 \) Abraham et al. 1999 also observe the normalised colour of red sequence galaxies, \( (g-r)_{t=19} \), to become increasingly blue with increasing cluster-centric radius, \( r_p \), as \( (g-r)_{t=19} = 1.05 - 0.079 \log r_p \).

These results indicate that the environment can affect the colour of a red sequence galaxy, so that red sequence galaxies are older and/or have higher metallicities in denser environments. To quantify this effect we consider a model red sequence galaxy as a 7.5 Gyr old (at \( z = 0.209 \), corresponding to 10 Gyr at the present epoch), \( \tau = 0.01 \) Gyr, solar-metallicity stellar population (Bruzual & Charlot 1993). By varying its age and metallicity independently, we find that to reproduce the observed reddening in the C-M relation, galaxies in the high-density region must be on average 500 Myr older or 20% more metal-rich than their intermediate-density counterparts. By studying the spectra of 22,000 luminous, red, bulge-dominated galaxies from the SDSS, Eisenstein et al. 2003 indi-
cate that red sequence galaxies in high-density regions are marginally older and more metal-rich than their counterparts in low-density environments, with both effects coming in at the same level.

This result is understandable in terms of cosmological models of structure formation, in which galaxies form earliest in the highest-density regions corresponding to the cores of rich clusters. Not only do the galaxies form earliest here, but the bulk of their star-formation is complete by $z \sim 1$, by which point the cluster core is filled by shock-heated virialised gas which does not easily cool or collapse, suppressing the further formation of stars and galaxies (Blanton et al. 1999, 2000). Diaferio et al. (2001) shows that as mixing of the galaxy population is incomplete during cluster assembly, the positions of galaxies within the cluster are correlated with the epoch at which they were accreted. Hence galaxies in the cluster periphery are accreted later, and so have their star-formation suppressed later, resulting in younger mean stellar populations. It should be considered however that this is a small-scale affect, and that this result in fact confirms that the red sequence galaxy population is remarkably homogeneous across all environments.

9.3. Galaxy Colours

As well as considering the effect of the cluster environment on galaxy morphologies and LFs, its effect on star-formation has been examined by numerous authors (e.g. Balogh et al. 2001, Ellingson et al. 2001, Lewis et al. 2002). They find that star-formation is consistently suppressed relative to field levels for cluster galaxies as far as twice the virial radius from the cluster centre, and that for the majority of galaxies in the cluster core star-formation is virtually zero. For photometric studies it is possible to qualitatively measure the effect of the cluster environment on star-formation through measurement of the blue galaxy fraction — the fraction of luminous ($M_R^* < -20$) galaxies whose colours indicate they are undergoing star-formation typical of late-type galaxies. We find that the blue galaxy fraction decreases monotonically with density, in agreement with other studies (e.g. Abraham et al. 1996, Kodama & Bower 2001).

The observed trends of steepening of the faint-end slope, faintening of the characteristic luminosity, and increasing blue galaxy fraction, from high- to low-density environments, are all manifestations of the well known morphology-density relation (Dressler 1980, Dressler et al. 1987), where the fraction of early-type galaxies decreases smoothly and monotonically from the cluster core to the periphery, while the fraction of late-type galaxies increases in the same manner. The observed trends in the composite LF simply reflect this morphology-density relation: the galaxy population in the cluster core is dominated by early-type galaxies and so the composite LF resembles that of this type of galaxy, with a shallow faint-end slope and a bright characteristic luminosity; whereas in lower density regions the fraction of late-type galaxies increases, and so the composite LF increasingly resembles that of the late-type TSLF, with a steep faint-end slope and a fainter characteristic magnitude (Binggeli et al. 1988).

Finally, we examined the effect of the cluster environment on galaxies through measuring the mean colour of luminous ($R < 21$) cluster galaxies as a function of their spatial position, as shown in Fig. 14. This shows more clearly than any other result, the complex effects of the cluster environment and dynamics on their constituent galaxies. A 209 appears a dynamically young cluster, with a significant elongation in the SE-NW direction, the result of a recent merger with smaller clumps. To measure the effect of the cluster dynamics on the galaxy population, their properties should be measured against the parameter most easily related back to the cluster dynamics, their spatial position. As the cluster is significantly elongated, it should be possible to distinguish between whether the local density or cluster-centric distance is more important in defining the properties of galaxies, and indeed it is clear that the mean galaxy colour correlates most with the local density rather than the distance of the galaxy from the cluster core. It should be considered through that as the system appears elongated due to being the merger of two or more clumps, the notion of a cluster-centric radius loses much of its validity, as where does the centre of the system lie during a cluster merger? The location of the main cluster and the secondary merging clump appear confirmed by Fig. 14, with the reddest galaxies concentrated around the cD galaxy (main cluster) and a more diffuse region 5 arcmin to the north coincident with the structure predicted from weak lensing analysis (Dahle et al. 2002). The effect of the preferential SE-NW direction for A 209 is apparent in the presence of bright blue galaxies near the cD galaxy perpendicular to the axis and hence unaffected by the cluster merger, and an extension of red galaxies to the SE which may indicate the infall of galaxies into the cluster along a filament. This preferential SE-NW direction appears related to the large-scale structure in which A209 is embedded, with two rich (Abell class R=3) clusters A222 at $z = 0.211$ and A223 at $z = 0.2070$ are located 1.5° (15 Mpc) to the NW along this preferential axis.

Cluster dynamics and large-scale structure clearly have a strong influence on galaxy evolution, and it would be interesting to search for direct evidence of their effect on the star-formation histories of galaxies through spectroscopic observations of galaxies in the secondary clump, in the form of post-starburst signatures.

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