Heralded quantum entanglement between two crystals

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Quantum networks must have the crucial ability to entangle quantum nodes\(^1\). A prominent example is the quantum repeater\(^2\text–}^4\), which allows the distance barrier of direct transmission of single photons to be overcome, provided remote quantum memories can be entangled in a heralded fashion. Here, we report the observation of heralded entanglement between two ensembles of rare-earth ions doped into separate crystals. A heralded single photon is sent through a 50/50 beamsplitter, creating a single-photon entangled state delocalized between two spatial modes. The quantum state of each mode is subsequently mapped onto a crystal, leading to an entangled state consisting of a single collective excitation delocalized between two crystals. This entanglement is revealed by mapping it back to optical modes and by estimating the concurrence of the retrieved light state\(^5\). Our results highlight the potential of crystals doped with rare-earth ions for entangled quantum nodes and bring quantum networks based on solid-state resources one step closer.

Quantum entanglement challenges our intuition about physical reality. At the same time, it is an essential ingredient in quantum communication\(^6\), quantum precision measurements\(^7\) and quantum computing\(^8\text–}^9\). In quantum communication, photons are naturally used as carriers of entanglement using either free-space or optical-fibre transmission. However, even with ultralow-loss telecommunication optical fibre, the transmission probability decreases exponentially with distance, limiting the achievable communication distance to a few hundred kilometres\(^10\). A potential solution is to use quantum repeaters\(^2\) based on linear optics and two quantum memories in a heralded manner\(^3\text–}^4\). Here, we present the observation of heralded quantum entanglement between two neodymium ensembles doped in two yttrium orthosilicate crystals (Nd\(_3\text{Y}_5\text{Si}_3\text{O}_{12}\)) separated by 1.3 cm (Fig. 1 and Methods). A nonlinear optical waveguide is pumped to produce photon pairs by means of SPDC. The resulting idler (1,338 nm) and signal (883 nm) photons are strongly filtered to match the working bandwidth of the crystals, yielding a coherence time of 7 ns. In the limit where the probability of creating a single pair is much smaller than one, the detection of an idler photon heralds the presence of a single signal photon. By sending the latter through a balanced beamsplitter, one heralds, neglecting optical losses, a single-photon entangled state\(^{26} 1/\sqrt{2}(|1\rangle_1|0\rangle_2 + |0\rangle_1|1\rangle_2\rangle)\) between the two spatial output modes \(A\) and \(B\). In each of the modes a crystal acts as quantum memory, denoted \(M_A\) or \(M_B\). Upon absorption of the single photon\(^{27}\), the detection of an idler photon heralds the creation of a single collective excitation delocalized between the two crystals, written as \(1/\sqrt{2}(|W_{AB}\rangle|0\rangle_A + |0\rangle_A|W_{AB}\rangle\). Here, \(|W_{AB}\⟩\) (or \(|W_{BA}\rangle\) is the Dicke-like state created by the absorption of a single photon in \(M_A\) (or \(M_B\)). To determine the presence of entanglement between the memories, we use a photon-echo technique based on an atomic frequency comb\(^{27\text–}^{31}\) that recovers the collective excitation into optical modes \(A\) and \(B\) after a preprogrammed storage time of 33 ns (with a total efficiency of 15\%). The resulting fields can then be probed using single-photon detectors to reveal heralded entanglement between the memories. As the entanglement cannot increase through local operations on the optical modes \(A\) and \(B\), the entanglement of the retrieved light fields provides a lower bound for entanglement between the two memories.

The photonic state retrieved from the memories is described by a density matrix \(\rho\), including loss and noise, expressed in the Fock state basis. To reveal entanglement in this basis, a tomographic approach based on single-photon detectors can be used\(^{32\text–}^{34}\). Specifically, from the values of the heralded probabilities \(p_{mil}\) of detecting \(m \in [0,1]\) photons in mode \(A\) and \(n \in [0,1]\) in mode \(B\), combined with the magnitude of the coherence between these modes, a lower bound on the concurrence \(C\) of the detected fields is obtained by

\[
C \geq \max(0, V(p_{01} + p_{10}) - 2\sqrt{p_{00}p_{11}})
\]

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and obtain a large concurrence, one should maximize second method based on twofold coincidences, which we for a lower probability of creating more than one pair). Hence, to observed. The prohibitively long integration time of this method by at least one standard deviation, which is consistent with the pres-

\[ p_{\text{obs}} = \frac{p}{1 + p} \]

...coherence between the retrieved fields in modes \(|A\rangle\) and \(|B\rangle\), as described in Supplementary Information). We therefore assume that the two-mode-squeezed state (TMSS) (see Methods and Supplementary Information). We present additional measurements that support our assumption about our source, and show that it leads to a lower bound on the concurrence. We performed a series of measurements for several values of the pump power, which is proportional to \( p \) provided \( p \ll 1 \). Figure 2a shows the interference of the delocalized single photon retrieved from the memories. The visibility does not depend on the pump power, and has an average value of \( 96.9 \pm 1.5\% \). Figure 2b shows the measured \( \bar{g}_{\text{corr}}(1) \) from which it can be seen that reducing the pump power increases the cross-correlation, as expected. Using additional measurements, we estimated the transmission loss, memory efficiency, dark count probability and pair creation probability of our set-up. These values were then used in a theoretical model (shaded region in Fig. 2b) that is in excellent agreement with the measured values of \( \bar{g}_{\text{corr}}(1) \), providing additional evidence that the estimated value of \( p_{11} \) yields a lower bound on the concurrence (see Supplementary Information). Figure 2c shows the lower bound on the concurrence for all pump powers, calculated using equations (1) and (2). The concurrence decreases with pump power because \( p_{11} \) increases, but all other terms in equation (1) depend on photon loss only and hence are approximately constant. Nevertheless, the concurrence remains larger than zero for all used pump powers, consistent with heralded entanglement between the atomic ensembles inside the two crystals. The results of the measurement of the concurrence based on twofold coincidences are plotted in Fig. 2c and agree, within uncertainty, with the results of the method based on measurement of the cross-correlation. The observed values of the concurrence are lower bounds on the amount of entanglement of the detected fields and are almost entirely determined by optical loss. Factoring out the detector inefficiency and interferometer loss yields a lower
approximately constant with an average of 96.5 from non-uniform loss after recombination of modes error bars are smaller than the symbols). The different amplitudes result

Figure 2 | Results. a, Visibility as a function of pump power. Visibility is approximately constant with an average of 96.5 ± 1.2% (green shaded region). Inset: visibility curves at 16 mW measured with detectors 1 (blue filled circles) and 2 (red open squares) (15 min acquisition time per point; error bars are smaller than the symbols). The different amplitudes result from non-uniform loss after recombination of modes A and B on the beamsplitter. The visibilities agree, within uncertainty, to the fits. b, Zero-time cross-correlation $g_{\Delta t}$ as a function of pump power. The decreasing values agree well with a theoretical model (shaded region; see Supplementary Information). c, Lower bound on the concurrence estimated using the cross-correlation measurement as a function of pump power (blue filled circles), calculated using equations (1) and (2), and the mean visibility of a. The concurrence decreases with pump power, as expected, but remains positive up to 16 mW. The shaded region corresponds to the model in b. All measured values of $p_{00}$, $p_{01}$, and $p_1$ are given in the Supplementary Information. All values are based on raw counts (that is, without subtraction of dark counts and accidental coincidences) and were obtained with coincidence detection windows of 10 ns. Uncertainties are obtained assuming Poissonian detection statistics. The lower bound on the concurrence at 16 mW obtained from measured threefold coincidences using either the MLE (green open diamond) or the CE (green filled diamond) are also shown (horizontally offset for clarity).

bound of ~0.01 for the concurrence of the field retrieved just after the crystals (see Methods).

The high interference visibility indicates that the stored entanglement does not significantly decohere during the 33 ns, and the coherent nature of the storage endures for longer times, as shown previously using storage of weak coherent states. Increasing the storage time does, however, lower the cross-correlation function $g_{\Delta t}$ as measured in ref. 23, and this should consequently lower the concurrence of the stored entanglement (this is essentially due to the decrease of the memory efficiency with increasing storage time, as shown in the Supplementary Information and in ref. 23). With Nd$^{3+}$:Y$_2$SiO$_5$ one could, in principle, store entanglement for up to ~1 μs (ref. 21). A promising approach to go beyond these limits, and to allow on-demand retrieval of the stored entanglement, is to implement spin-wave storage to increase the storage times (as demonstrated recently in Pr$^{3+}$:Y$_2$SiO$_5$), and to place the crystal inside an impedance-matched cavity to increase the efficiency. Such improvements are necessary for the development of a quantum repeater based on solid-state quantum memories, and are the subject of current research.

In conclusion, we have reported an experimental observation of heralded quantum entanglement between two separate solid-state quantum memories. We emphasize that although the entangled state involves only one excitation, the observed entanglement shows that the stored excitation is coherently delocalized among all the neodymium ions in resonance with the photon, meaning $\sim 1 \times 10^{10}$ ions in each crystal. Our results demonstrate that RE ensembles, naturally trapped in crystals, have the potential to form compact, stable and coherent quantum network nodes. Moreover, single-photon entanglement is a simple form of entanglement that can be used for teleportation and entanglement swapping operations and can also be purified using linear optical elements. It is also a critical resource in several proposals for quantum repeaters, as it is less sensitive to transmission loss and detector inefficiencies. This, however, is counterbalanced by the extra requirement of phase stabilization over long distances, and the duplication of the resources for post-selecting entanglement shared between two photons, which is needed to implement qubits measurements. Our experimental approach is based on solid-state devices, the key components being the PPKTP chip (the photon source) with an integrated waveguide and the crystal memory. We believe that this approach opens up possibilities for the integration of components, such as frequency filtering directly on the chip or waveguide quantum memories. The prospect of combining solid-state photon sources and quantum memories is therefore attractive for practical future quantum networks. One important challenge in this context is to create entanglement between two remote solids in a heralded way using two distant sources of photon pairs and a central station performing a single-photon Bell state measurement, that is, the realization of an elementary link for quantum repeaters.

Methods

Experimental set-up and concurrence estimation. To reveal entanglement in the Fock basis, one cannot resort to violating a Bell inequality given solely inefficient and noisy single-photon detectors. Instead, quantum state tomography using single-photon detectors was developed. Implicit to this method are the assumptions that (i) the creation of more than two pairs is negligible and (ii) the off-diagonal elements of $\rho$ with different number of photons vanish (this is valid because no local oscillator providing an aphase reference was used; ref. 5). To estimate $\langle V_{0,0} \rangle$, $\langle V_{0,1} \rangle$ and $\langle V_{1,4} \rangle$, we used the set-up of Fig. 1 in the following way. First, the visibility $V$ was measured by allowing the re-emitted delocalized photon to interfere with itself using a balanced Michelson interferometer for which the phase was actively stabilized. We then blocked spatial mode $B$ to estimate $p_{01}$ by summing the number of detections on detectors 1 and 2, conditioned on a heralding signal. This is justified, as the probability of creating two photon pairs is much smaller than the probability of creating a single one. Probability $p_{01}$ is estimated similarly by blocking mode $A$ instead of $B$. Alternatively, we could also estimate the sum $p_{01} + p_{10}$ directly by randomizing the phase of the interferometer, with both arms unblocked (further clarifications and justifications on these measurements are
given in the Supplementary Information). Then, $P_0$ is estimated through normalization of the total probability, $P_0 \approx 1$, which is justified by the fact that $P_1 \ll P_0$. Consequently, $P_1 \gg P_0$.

The estimation of $P_1$, using the cross-correlation, which is motivated by the results of ref. 13, assumes that all the observed detections stem from a TMSS. In the Supplementary Information, we show that this assumption is conservative and that it yields a lower bound for the concurrence. Using the cross-correlation to estimate $P_1$ requires only the measurement of twofold coincidences, rather than threefold coincidences as for the other method. For our specific set-up, this resulted in a reduction of the measurement time by a factor of $10^{6}$ to achieve a similar statistical confidence on the concurrence. Moreover, this method requires no physical modifications to the optical circuit to measure different components of the retrieved fields, which simplifies its implementation. In the Supplementary Information, we present additional measurement that provide evidence that our source produces a state that is very close to an ideal TMSS, and we summarize the results here. We measured the second-order autocorrelation of the signal (or idler) mode without storage to be $g_{2}(0) \approx 1.82(1)$ (or $g_{2}(0) \approx 1.86(9)$), which is very close to the maximal value of 2 associated with the thermal photon statistics (the lower observed value can be entirely attributed to the finite temporal resolution of our detectors). We also measured the zero-time second-order autocorrelation function of the heralded signal photon just before storage and obtained $g_{2}^{(0)}(0) = 0.061(4)$ for a pump power of 8 mW, which is consistent with $p \approx 1$.

The observed values of the concurrence are lower bounds on the amount of entanglement of the detected fields and are almost entirely determined by optical loss. To see this, we first note that when both the multi-pair creation probability and the total transmission probability of each single photon are small, the concurrence is approximately given by $C \approx \eta \sqrt{2 - 1/(g_{2}^{(0)} - 1)}$. At 8 mW of pump power, we measured $g_{2}^{(0)} \approx 10$, $P_0 = 0.99783(71)$ and $P_1 = 5.18(40) \times 10^{-5}$, and hence $C \approx 0.39$. With $\eta \approx 0.39$, $P_0 = 2.2 \times 10^{-5}$, we see that $C \approx 6.6 \times 10^{-5} \ll 0.3$. Using this, an estimate of the concurrence of the fields retrieved just after the crystals is obtained by noticing that the transmission $\eta$ is the product of the probability to find the signal photon inside the fibre per heralding signal (20%), the memory efficiency (15%), the transmission in the interferometer (2.4%) and detector efficiency (30%). Factoring out the detector inefficiency and the interferometer loss yields a lower bound of $\sim 0.01$ for the concurrence of the field retrieved just after the crystals.

All results were derived from raw counts, that is, without the subtraction of dark counts and accidental coincidences, and were obtained with coincidence detection windows of 10 ns. We note that there is no measurable temporal overlap between stored and transmitted photons, and that the transmitted photons do not contribute to the entanglement (see Supplementary Information for details, where histograms showing the temporal profiles of detected photons are shown).

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Author contributions

All authors conceived the experiment. I.U., C.C. and F.B. performed the measurements. I.U., C.C., F.B., N.S. and M.A. analysed the data. All authors contributed to the writing of the manuscript. I.U., C.C. and F.B. contributed equally to this work.

Additional information

The authors declare no competing financial interests. Supplementary information accompanies this paper at www.nature.com/naturephotons. Reprints and permission information is available online at http://www.nature.com/reprints. Correspondence and requests for materials should be addressed to M.A.