The Implementation of Quasi-Z-Source Four-Leg Inverter with PV by using Model Predictive Control Scheme is proposed in this paper. In order to reduce the drawbacks of traditional three phase voltage source inverter (VSI). Photovoltaic (PV) is a term which converts the light into electricity. This topology features a wide range of voltage gain which is suitable for applications in renewable energy-based power systems, where the output of the renewable energy sources varies widely with operating conditions such as wind speed, solar irradiation and temperature. To improve the capability of the controller, an MPC scheme is used which implements a discrete-time model of the system. The controller handles each phase current independently, which adds flexibility to the system. The performance of quasi z source three-phase four-leg VSI with PV by using model predictive control (MPC) was simulated using MATLAB Simulink under balanced and unbalanced load conditions as well as single-phase open-circuit fault condition.

Keywords: DC-AC Power Conversion, Four-Leg Inverter, PV Array, Model Predictive Control (MPC), Quasi-Z-Source Inverter (QZSI).

I. INTRODUCTION

Now a days the demand of conventional energy sources increasing, in order to reduce this demand an alternative energy sources that’s why renewable energy sources can be used. Renewable energy sources are wide spread, freely accessible, less maintenance, less the cost of operation and no impact on environment. Due to above advantages of renewable energy sources are used in various applications such as distributed generation, power unavailable areas, off grid and emergency situation.

However renewable energy can be converted into electrical distribution systems need power electronic converters. The performance of all these RES thus depends on the power electronic converters and control method [1].In most of applications to supply the power to either the local loads or the grid a three-phase voltage-source inverters are used. But it has two disadvantages they are 1) variation of input voltage and 2) output unbalanced current.

The variation of this input voltage due to random and sporadic nature of RES this is first disadvantages of disadvantage of VSI .The VSI must have input voltage is greater than the maximum value of the line to line output voltage in order to vouch reliable and continuous power for the loads, which is a major dispute in such systems. To overcome this drawback a dc - dc chopper is used at the input stage to supply
the regulated voltage for the voltage source inverter. However, by using this chopper circuit engrossment increases and require multi loop control structure which makes high cost and lower reliability.

The alternative method to VSI is a current source inverter (CSI). In CSI without using dc to dc chopper to enhancing voltage. The CSI also has two drawbacks they are 1) the output voltage cannot be lower than the dc input voltage. 2) To avoid the open circuit of all upper switching devices or all lower devices a Overlap time between phase legs is required. Otherwise, an open circuit of the dc inductor would ensue and extinguish the devices. Furthermore in CSI for safe current commutation overlap time is desired, which causes waveform deprivation [3]. To avoid these problems recently a new power converter topologies have been proposed [4]. The quasi-impedance source inverter can overcome the above-mentioned problems. It employs a unique impedance network (or circuit) to couple the converter main circuit to the power source, load for providing unique features that cannot be observed in the traditional VSI and CSI source converters. This is the simple L–C network to achieved buck–boost functionality in single-stage power conversion.

The three-phase VSI are usually designed for balanced three-phase loads, this is the second disadvantage of VSI. However, in distribution power generation system unbalanced load conditions are common where power is delivered to local loads. Due to these unbalanced loads current circulating flow in power system Causing swelter of the neutral line and harmonic distortion on the output voltage [8], [9]. One way to relieve this problem a three-phase four-leg VSI is used. This network can produce for even nonlinear and unbalanced loads three-phase balanced output. This is the best method for UPS systems and individual power generation systems.

The reliable and efficient operation of the renewable energy-based power generation systems depends on the control scheme of the power converter which plays a important role. There are a number of proposed control strategies for the QZSI. In most applications, proportional integral (PI) controller is used to control current, voltage, etc. but it has some drawbacks. The major drawback is entire system performance depends on the inner control loop performance. To generate PWM signals for the power switches the controller needs a modulator, such as 3-D-SVPWM to implement the desired control action.

The alternative controller for QZSI is model predictive control (MPC) which is having wild vigorous response, simple concept, and capacity to include different non linearity’s and limitations. The major advantage of MPC is without using modulation stage a direct control action to the converters. In most of applications MPC is used in multilevel inverters, traditional three-phase inverter, and a number of electrical drives for current control.

In these presents Implementation of Quasi-Z-Source Four-Leg Inverter with Model Predictive Control Scheme for Renewable Energy Based Power Systems. The assistances of this study are shortened as monitors.

1. To minimize the drawbacks of three phase traditional VSI and two-stage power conversion by using the QZS network instead of a dc–dc + dc–ac converter.
2. The reliable operation of renewable energy-based power system under balanced and unbalanced load conditions using three-phase four-leg inverter.
3. The control of load current and QZS network capacitor voltage using MPC scheme with high precision and wild response.
4. The proposed MPC controller knobs apiece phase current independently. Due to this QZS four-leg inverter offers fault-tolerant capability.

II. MODEL OF QZS FOUR LEG INVERTER WITH PV

2.1 Topology

The QZS four-leg inverter with R–L filter connect to PV input as shown in Fig.1. This topology can be explored as three parts: 1) Photo voltaic source 2) QZS network and 3) four-leg inverter with R–L filter and load. In the first part of this topology Photovoltaic (PV) is a term which converts the light into electricity. In the second stage of this topology the QZS is made of LC network in the shoot through state both devices are gated at the same time. During this state, energy can be transferred from the capacitors to the inductors in QZS network.

In the third part of this topology, the four-leg VSI inverter is used. As shown in Fig. 1, the neutral load point is connected to the mid-point of the VSI inverter’s fourth phase leg to tolerate for zero voltage or current sequence. But it has one major drawback is switching organizations are more complicated compared to a three phase three leg VSI due to extra fourth leg. By using an extra fourth leg to improve the VSI inverter ability, consistency and also it is operated under balanced or unbalanced or linear or nonlinear load conditions.

The QZS network of equivalent circuits as shown in Fig. 2(a) and 2(b), respectively [33] in this analysis PV consider as dc voltage source. When it is operated in shoot through state and non-shoot-through states. In this figures all voltages and currents are shown with arrows and the polarities.

2.2.1 Non shoot-through state

The four-leg inverter network is represented by a constant current source when it is operated during non-shoot through state as shown in below fig 2(a).

By applying in above Fig. 2 Kirchhoff’s voltage law (KVL), voltage of inductors (VL1 and VL2), dc-link voltage (VPN), and diode voltage (Vdiode) are written as

\[ V_{L1} = V_{in} - V_{C1} \]
\[ V_{L2} = -V_{C2} \]  \hspace{1cm} \ldots \ldots (1)
\[ V_{PN} = V_{C1} - V_{L2} = V_{C1} + V_{C2} \] \hspace{1cm} \ldots \ldots (2)

2.2.2 Shoot-through state

The four-leg inverter network is represented by short-circuit, when it is operated during shoot through state as shown in below fig 2(b).

\[ V_{L1} = V_{in} - V_{C1} \]
\[ V_{L2} = -V_{C2} \]  \hspace{1cm} \ldots \ldots (1)
\[ V_{PN} = V_{C1} - V_{L2} = V_{C1} + V_{C2} \] \hspace{1cm} \ldots \ldots (2)
By applying in above Fig. 3 Kirchoff’s voltage law (KVL), voltage of inductors (VL1 and VL2), dc-link voltage (VPN), and diode voltage (Vdiode) are written as

\[ V_{L1} = V_{in} + V_{C2} \quad V_{L2} = V_{C1} \quad \ldots (3) \]
\[ V_{diodet} = V_{C1} + V_{C2} \quad V_{PN} = 0 \quad \ldots (4) \]

The network operated at steady state over one switching cycle, the average capacitor voltages are

\[ V_{C1} = \frac{T_1}{T_1-T_0}V_{in} \quad V_{C2} = \frac{T_0}{T_1-T_0}V_{in} \quad \ldots (5) \]

Where \( T_0 \) is the shoot-through state period, \( T_1 \) is the non-shoot-through state period, and \( V_{in} \) is the input dc voltage.

From (2), (4), and (5), equations the peak dc-link voltage across the inverter bridge in Fig. 1 is

\[ V_{PN} = V_{C1} + V_{C2} = \frac{T}{T_1-T_0}V_{in} = BV_{in} \quad \ldots (6) \]

Where \( B \) is the boost factor of the QZSI, and \( T \) is the switching cycle \((T_0 + T_1)\). The average inductor currents \( L1 \) and \( L2 \) are

\[ i_{L1} = i_{L2} = I_{in} = \frac{P}{V_{in}} \quad \ldots \ldots \ldots (7) \]

Applying Kirchoff’s current law (KCL) in above figures and (7) results in

\[ i_{c1} = i_{c2} = i_{PN} - i_{L1} \quad \ldots \ldots (8) \]

From above all equations voltage gain \((G)\) of the QZSI can be expressed as

\[ G = \frac{V}{0.5V_{PN}} = MB \quad \ldots (9) \]

Where \( M \) is the modulation index and \( V \) is the peak phase voltage

### 2.3 Mathematical analysis of the Four-Leg Inverter

The four-leg inverter with the output R–L filter equivalent circuit as shown in Fig. 3

[Diagram of four-leg inverter]

Where the \( L_{fj} \) is the filter inductance, \( R_{fj} \) is the filter resistance, and \( R_j \) is the load resistance for each of the phase \( j = a, b, c \).

By adding fourth leg to the three-phase four-leg inverter which makes the switching states 16. The valid switching states of four leg inverter with the corresponding phase and line voltages are presented in [34]. In addition to fourth leg one more switching state is needed in order to operate in shoot through state. Therefore in this application a total number of 17 switching states are used.

The four-leg inverter of each leg voltage can be expressed as

\[ V_{aN} = S_aV_{dc} \quad V_{bN} = S_bV_{dc} \quad V_{cN} = S_cV_{dc} \quad V_{nN} = S_nV_{dc} \ldots (10) \]

Where \( S_a, S_b, S_c, \) and \( S_n \) are the switching states of four-leg inverter, \( V_{dc} \) dc link voltage, and \( V_{nN} \) load neutral voltage.

The inverter output voltage can be expressed in terms of the previous voltages of inverter

\[ V_{an} = (S_a - S_n)V_{dc} \quad V_{bn} = (S_{ab} - S_n)V_{dc} \]
\[ V_{cn} = (S_c - S_n)V_{dc} \quad \ldots \ldots (11) \]
The voltages of inverter can be stated in terms of load-neutral voltages and currents by applying Kirchhoff’s voltage law (KVL) to Fig. 3

\[ V_{AN} = (R_{fa} + R_a) i_a + L_{fa} \frac{d i_a}{dt} + V_{nN} \]

\[ V_{BN} = (R_{fb} + R_b) i_b + L_{fb} \frac{d i_b}{dt} + V_{nN} V_{CN} = (R_{fc} + R_c) i_c + L_{fc} \frac{d i_c}{dt} + V_{nN} \ldots (12) \]

From equations (11) and (12), the output voltages can be written as

\[ V_{an} = (R_{fa} + R_a) i_a + L_{fa} \frac{d i_a}{dt} V_{bn} = (R_{fb} + R_b) i_b + L_{fb} \frac{d i_b}{dt} \]

\[ V_{cn} = (R_{fc} + R_c) i_c + L_{fc} \frac{d i_c}{dt} \ldots (13) \]

Equation (13) can be simplified to

\[ V_j = (R_{fj} + R_j) i_j + L_{fj} \frac{d i_j}{dt} j = a, b, c \ldots (14) \]

An the neutral load current in can be written as

\[ i_n = i_a + i_b + i_c \ldots (15) \]

From equation (14) the output current can be expression as

\[ \frac{d i_j}{dt} = [V_j - (R_{fj} + R_j) i_j] \frac{1}{L_f} j = a, b, c \ldots (16) \]

III. PROPOSED MPC

The block diagram of the proposed MPC scheme is shown fig 4. It is mainly divided into two layers: 1) a predictive model and 2) cost function optimization. To predict future behavior of the control variables using discrete-time model of the system. To minimize the error between the reference and the predicted control variables used the cost function in the next sampling time. This MPC control technique has many advantages are to implement for both linear and nonlinear systems, high precision and wild dynamic response [35].

Figure 5.

3.1 predictive model : This is used to estimate the future behavior of each of the output currents (ia, ib, ic). By substituting equation (18) into (16) the each output phase current in

Discrete time model is

\[ i_j(k + 1) = A_i v_j(k + 1) + A_i i_j(k), j = a, b, c \ldots (19) \]

Where \( i_j(k + 1) \) is the predicted output current at the next sampling time and \( A_i \) and \( A_i \) are constants are defined by

\[ A_i = \frac{T_s}{L_f + (R + R_f)T_s} A_i = \frac{L_f}{L_f + (R + R_f)T_s} \ldots (20) \]

The continuous capacitor current can be stated as

\[ i_{c1} = C_1 \frac{d (V_{c1} - i_{c1} r_c)}{dt} \ldots (21) \]

Where \( C_1 \) is the capacitance, \( r_c \) is the equivalent series resistance (ESR) of the capacitor from equation (21) the capacitor voltage is

\[ \frac{d V_{c1}}{dt} = r_c \frac{d i_{c1}}{dt} + \frac{i_{c1}}{C_1} \ldots (22) \]

By substituting equation (18) into (22), the VC1 can be written as
\[ V_{c1}(k+1) = V_{c1}(k) + i_{c1}(k+1)r_c + i_{c1}(k)\left(\frac{V_c}{c} - r_c\right) \]  
\[ g(k+1) = g_1(k+1) + g_v(k+1) \]  
\[ i_{c1} = I_{L1} - (s_a i_a + s_b i_b + s_c i_c) \]  
\[ i_{c1} = -I_{L1} \]  

3.2 optimization of Cost function

The selection of cost function in MPC scheme plays an important role. The proposed MPC scheme has mainly two cost functions they are 1) to reduce the output current error and 2) capacitor voltage error in the next sampling time. The cost function of output current is defined as

\[ g_i = \left( i_j^*(k+1) - i_j(k+1) \right)^2 = (i_a^*(k+1) - i_a(k+1))^2 + (i_b^*(k+1) - i_b(k+1))^2 + (i_c^*(k+1) - i_c(k+1))^2 \]  

Where \( i_j^*(k+1) \) is the output reference current, \( i_j(k+1) \) is the output predicted current vector in the next step (\( j = a, b, c \)).

The capacitor voltage in cost function can be defined as

\[ g_v = \lambda \times |V_{c1}^*(k+1) - V_{c1}(k+1)| \]  

Where \( V_{c1}^*(k+1) \) is the reference capacitor voltage and \( V_{c1}(k+1) \) is the predicted capacitor voltages. The overall cost function is

\[ \text{Minimization of Cost Function} \]

3.3 Control algorithm

The proposed control algorithm of flowchart is shown in Fig. 5. The Cost function minimization is executed for each voltage vector to predict the values reaped, calculate the cost function, and store the very low value and the index value of the corresponding each switching state. The control algorithm of proposed system can be concise in steps.

1) Sampling the phase output currents (iabc), inductor current (iL1), and capacitor voltage (VC1).
2) The above parameters are used to output predict currents and capacitor voltage using the predictive model of proposed system 3.1, and 3.2, respectively.
3) Calculate all predictions using complete cost function.
4) The minimum voltage vector corresponds to the optimal switching state that reduces the cost function is designated to be applied at the next sampling state.

### IV. Simulation results of proposed MPC technique of QZS four-leg inverter

#### 4.1 steady state analysis

The QZS network reference capacitor voltage \((V_{c_1}^*)\) is set to 150 V and input voltage is 100 V to perform the steady-state analysis. The following two cases are considered to show the effectiveness of the proposed controller under steady-state operation.

1) **Case-1**: Balanced reference currents \((i_a^* = i_b^* = i_c^* = 10\, \text{A})\) and balanced loads \((R_a = R_b = R_c = 7.5\, \Omega)\).
2) **Case-2**: Unbalanced reference currents \((i_a^* = 10\, \text{A}, i_b^* = 5\, \text{A}, i_c^* = 5\, \text{A})\) and balanced loads \((R_a = R_b = R_c = 10\, \Omega)\).

The neutral current, which is the sum of the three-phase load currents, is zero in cases of balanced reference current [see Fig. 7. (a)]. On the other hand, the neutral current flows through the fourth leg of the inverter in case of the unbalanced reference current [see Fig. 7. (b)]. It can be observed that the inductor current \((i_{L1})\) remains continuous, which significantly reduce the input stress.

#### 4.2 Transient-State Analysis

To perform the transient-state analysis the reference output currents step from 5 to 10 A are shown in Fig. (a). For this test, reference loads \((R_a = R_b = R_c = 6\, \Omega)\) are balanced. It can be seen that the output currents track to the references with fast rise time and no overshoot. In Fig. (b), the results are presented with unbalanced reference current step change and balanced loads \((R_a = R_b = R_c = 6\, \Omega)\). For this test, all reference output currents are set to 5 A at the beginning. Then, reference currents are set to \(i_a^* = 7\, \text{A},\)
$i_p = 10A$, and $i_c = 12A$. Results of this test show that the proposed controller handles each phase current independently and the output currents (ia, ib, ic) and the capacitor voltage (VC1) track their references and the dc-link voltage (VPN) is kept constant. However, the double line frequency (2*fo) ripple exist on the QZS network due to unbalanced current. The simulation results of transient-state analysis with balanced and unbalanced reference currents are shown in Fig. 8. (a) and (b), respectively.

![Figure 8. (a)](image1)

![Figure 8. (b)](image2)

### 4.3 Analysis of Fault-Tolerant Capability

The proposed system is also tested for a fault condition, which may occur during the operation of the three-phase inverters. To do that, one-phase is made an open circuit and the corresponding reference current ($i_p$) is set to 0 A. The transient state simulation results are shown in Fig. 11(a). The stability of the QZS network deteriorated after single-phase fault. The inductor current is discontinuous that increases the input stress, and the output current waveforms affected from the fault. Furthermore, the output current of THD is higher than previous case, as shown in Fig. 12(b). As a result of this test, the proposed QZS four-leg inverter offers much better fault-tolerant capability than traditional three-phase inverter.

![Figure 9](image3)

### V. CONCLUSION

This paper has proposed the Implementation of Quasi-Z-Source Four-Leg Inverter with PV by using Model Predictive Control Scheme. The main aim of this paper is to achieve single-stage power converter topology for photo voltaic system under balanced and unbalanced conditions with high control capability. To do that, QZS three-phase four-leg inverter topology was proposed in this study. To improve control capability of the controller, the MPC scheme was employed in the controller stage. The performance of the proposed inverter topology and its control strategy was simulated. The results show that the proposed technique not only has an excellent steady-state and transient performances, but also it is robust against fault conditions.
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