High-temperature short-range order in Mn₃RhSi

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Conventional phase transitions are well understood in terms of the order parameter, based on the Landau-Ginzburg-Wilson theory. However, unconventional magnetic orders have been observed in clean systems such as MnSi. The unconventional magnetic orders of conduction electrons in the metallic phase has been observed for high-temperature superconductors and heavy fermion compounds. However, these unconventional magnetic orders have been limited to relatively low temperatures as quantum phase transitions. Here high-temperature magnetic short-range order is observed as one of the unconventional magnetic orders at temperatures up to 720 K in a noncentrosymmetric intermetallic antiferromagnet Mn₃RhSi with a well-ordered lattice. The magnetic Mn ions form a hyperkagome network of corner-sharing triangles, where the spins are geometrically frustrated. The spin network is equivalent to that of a spin liquid and non-Fermi-liquid material, β-Mn. Our observation indicates that a metallic phase with magnetic short-range order exists at high temperatures.
Unconventional magnetic order of conduction electrons has been observed in a paramagnetic metallic state of MnSi under pressure by neutron diffraction and μSR measurements. The similar unconventional magnetic order has been observed near the magnetic transition temperatures of inhomogeneous chiral-spin states in MnSi and FeGe. As another case of unconventional magnetic order, solitonic spin liquid (SL) has been reported in an incommensurate magnetic phase of Fe1−xTe in a very narrow temperature range above the Néel temperature, as observed by a local magnetic probe, Mössbauer spectroscopy. An inhomogeneous magnetic ordered state has also been observed in a triangular lattice magnet, α-NaMnO3, with nanometer-scale phase separation far below room temperature. The origin of this order is attributed to local symmetry breaking by defects in the crystal structure. In addition, magnetic fragmentation has been reported for the spin ice compound Nd2Zr2O7 below 1 K, where the tetrahedral network is symmetry broken by defects in the crystal structure. In addition, liquid (SL) has been reported in an incommensurate magnetic another case of unconventional magnetic order, solitonic spin configuration accompanied by a small ferromagnetic component normal to the triangular plane. The triangle units form a helical spin rod along the [111] direction, which results in a geometrically frustrated hyperkagome structure. The Mn magnetic moment at T = 4 K is estimated as 2.61 ± 0.03 μB. In addition to the magnetic Bragg peaks, strong diffuse scattering is observed near Q = 1−1.7 Å−1, as shown in Fig. 2a. This scattering is not observed in the X-ray diffraction pattern in Fig. 2b or the electron diffraction patterns (Supplementary Note 2, Supplementary Fig. 3), confirming its magnetic origin. The Q position is precisely identical to the previously observed magnetic diffuse scattering position for SL in β-Mn0.8Co0.2 (21) or spin glass (SG) in β-Mn1−xInx (20). The original β-Mn is a well-known SL material with a three-dimensional hyperkagome network of triangular Mn spin units. Non-Fermi-liquid (NFL) behavior is also indicated in β-Mn based on the exponent of the temperature dependence of the resistivity and the scaling of the dynamical spin susceptibility. The magnetic diffuse scattering remains at T = 4 K, suggesting the coexistence of two types of magnetic orderings with different coherence lengths at different Q positions. The magnetic diffuse scattering intensity increases as the temperature increases up to \( T_N \). The integrated intensity is estimated as ~0.8 μJ at 4 K and increases to ~1.3 μJ at 300 K, based on the reverse Monte Carlo simulation reported in ref. (Supplementary Note 3). However, the magnetic diffuse scattering remains at temperatures above \( T_N \), persisting to ~700 K, as shown in Fig. 3a. According to an isotropic short-range spin correlation model analysis (Supplementary Note 4), the SRO spin correlation primarily consists of an antiferromagnetic (AFM) correlation between the first NN spins and a ferromagnetic correlation between the fifth NN spins, as reported in ref. 21.

The observed diffuse scattering of Mn1RhSi can be attributed to a SRO. To estimate the volume fraction of the SRO in Mn1RhSi, μSR measurements were performed. μSR is a unique tool that can reveal the SRO volume fraction. This tool has been successfully applied for studies of phase separations in materials near the quantum phase transition. In addition, the spin-lattice relaxation rate of μSR assists in our assessment of the magnetism.
In Mn$_3$RhSi, the SRO was observed as a decrease in the normalized initial asymmetry in the paramagnetic phase. The temperature dependence of the magnetic volume fraction over the whole volume is shown in Fig. 3b, following the estimation methods described in the methods (muon spin relaxation measurements). The volume begins to increase as the temperature decreases below 720 ± 21 K. In contrast, the muon spin relaxation rate, $\lambda$, of the remaining paramagnetic component exhibits Curie–Weiss behavior, as shown in Fig. 3c, where the Weiss temperature roughly corresponds to $T_N$.

In the paramagnetic region, magnetic diffuse scattering appears gradually, with the $\mu$SR measurement showing a linear increase in SRO volume fraction with decreasing temperature. These different temperature dependences suggest that the magnetic moment in the SRO state gradually develops with decreasing temperature.

Based on the $\mu$SR measurement (Supplementary Note 5), the SRO volume fraction was 22.9% at $T = 300$ K. According to neutron diffraction measurements at $T = 4$ K, the ordered magnetic moment was 2.61 $\mu_B$, whereas the magnetic moment of the diffuse scattering was approximately 0.8 $\mu_B$. The total magnetic moment reaches 2.73 $\mu_B$ at 4 K. As the temperature increases to 300 K, only the magnetic moment of diffuse scattering remains at 1.3 $\mu_B$. Based on the 22.9% SRO volume fraction at 300 K, the total magnetic moment is expected to decrease from 2.73 $\mu_B$ at 4 K to 1.31 $\mu_B$ at 300 K. This value of 1.31 $\mu_B$ is almost the same as the observed value of 1.3 $\mu_B$ by neutron diffuse scattering at 300 K. This coincidence suggests that the magnetic moment is transferred from the SRO to the long-range order at the other Q position on cooling below the Néel temperature.

One may suspect that the magnetic diffuse scattering may be induced by disorders such as local defects or elemental substitutions at individual sites in the crystal structure. In addition, not only the magnetic structure but also the crystal structure may be phase-separated, as observed in the triangular lattice magnet α-NaMnO$_3$. The crystal structure of Mn$_3$RhSi was studied by both neutron and X-ray diffraction measurements, and neither defects nor elemental disorders were identified in the range of 3σ (Supplementary Note 1, Supplementary Table 1). However, nuclear diffuse scattering may be included in Fig. 2a, as observed at $Q = 0.8$ Å$^{-1}$ for $\beta$-Mn$_3$In$_2$. In the case of Mn$_3$RhSi, nuclear diffuse scattering at $Q = 0.8$ Å$^{-1}$ is not observed in the X-ray diffraction pattern, as shown in Fig. 2b. Our electron diffraction measurement shows diffuse scattering peaks at $\{1/2 1/4 2\}$ as the lowest reciprocal point, which corresponds to $Q = 2.01$ Å$^{-1}$ (Supplementary Note 2, Supplementary Fig. 3). This diffuse scattering is not observed in the X-ray diffraction pattern of Fig. 2b, possibly due to its weak intensity. The diffuse scattering intensity significantly decreased from $T = 100$ K to 300 K, suggesting that the lattice strain may disappear above 300 K. Based on these results, we conclude that the SRO does not originate from disorder.

The SRO in this new compound, Mn$_3$RhSi, is confirmed by a complementary use of neutron diffraction, X-ray diffraction, electron diffraction, and $\mu$SR measurements in this work. The SRO effect is manifested in the physical properties of Mn$_3$RhSi as follows. The temperature dependence of the magnetic susceptibility of Mn$_3$RhSi exhibits non-Curie–Weiss behavior over a wide temperature range from the long-range magnetic transition temperature ($T_N = 190$ K) to ~700 K (Fig. 4a). The detailed study of the magnetic susceptibility is shown in Supplementary Note 6.
As a possible origin of this non-Curie–Weiss behavior, one may consider a possible coupling of localized spins and conduction electrons as the Kondo effect in this compound. However, the low-temperature specific heat capacity does not show any significant enhancement of the electron mass, as illustrated in Fig. 4b. The estimated Sommerfeld constant $\gamma$ is 12.18 $\pm$ 0.03 mJ Mn$^{-1}$K$^{-2}$, while $\beta$-Mn is known as a heavy 3$d$ electron material with a Sommerfeld constant of 70 mJ Mn$^{-1}$K$^{-2}$ 24. $\beta$-Mn shows a broad peak at ~140 K in the temperature dependence of the magnetic susceptibility, which may correspond to the Kondo temperature. Based on the specific heat results, we conclude that the Kondo effect is not the origin of this non-Curie–Weiss behavior. Some low-dimensional magnets also show a hump structure in the magnetic susceptibility, such as Bonner–Fisher-type magnets 25. However, the present compound is a three-dimensional cubic magnet. The critical exponent of the temperature dependence of the Mn magnetic moment is close to 1/3, conforming to the classical model of a three-dimensional magnet. The solid line in Fig. 5 is a least-squares fit to the ordered magnetic moment based on the classical power-law function expressed as $\mu(T) = \mu_0 (1 - T/T_N)^\beta$. The fitting gives a long-range magnetic transition temperature of 190.1 $\pm$ 0.2 K and a critical exponent $\beta$ of 0.28 $\pm$ 0.03. The obtained transition temperature is consistent with that of the magnetic susceptibility measurement. The critical exponent suggests a second-order-type phase transition, with three-dimensional spin interactions corresponding to the Ising, XY, or Heisenberg model in Mn$_3$RhSi 26. This result excludes the possibility of Bonner–Fisher-type magnetic susceptibility in the paramagnetic region. Based on these results, the origin of the present non-Curie–Weiss temperature dependence can be attributed to the SRO effect.

Similar ternary cubic compounds, such as Mn$_3$TX (T = Co, Ir; X = Si, Ge) 17–19, have primarily been characterized with respect to their crystallographic and long-range ordered magnetic structure. The published data are inconclusive regarding possible SRO in these series, but non-Curie–Weiss behavior and broad magnetic diffuse scattering signals in neutron powder diffraction patterns above the ordering temperature may warrant further research on these compounds. Results for the series of compounds with the $\beta$-Mn structure suggest that Mn$_3$RhSi is located near a quantum critical point between a SL state and a long-range AFM ordered state, as shown in Fig. 6, where the long-range magnetic transition temperature decreases as the lattice constant decreases toward the quantum critical point. As the lattice constant decreases, the electronic bandwidth $W$ increases. Therefore, the decrease in $T_N$ with decreasing $U/W$ is consistent with the theoretical expectation for an AFM metal. However, some variations in $T_N$ are shown for the different systems in Fig. 6, suggesting that other parameters, such as the DM interaction, are required to describe this phase diagram. In this sense, there may be a quantum multicritical point 24 that depends on the bandwidth, the DM interaction, and other parameters such as the Fermi surface topology. Our remarkable finding is the widely spread unconventional magnetic SRO up to 720 K, as illustrated in Fig. 6. Although this SRO state has not been confirmed in other compounds, magnetic diffuse scattering has been observed in $\beta$-Mn 24, $\beta$-Mn$_{0.8}$Co$_{0.2}$ 21, $\beta$-Mn$_{1.3}$In$_{0.2}$ 20, and $\beta$-Mn$_{1.3}$Al$_{0.2}$ 23. Notably, diffuse scattering occurs in $\beta$-Mn$_{0.8}$Co$_{0.2}$, but the intensity decreases with decreasing temperature, and almost disappears at low temperatures. For $\beta$-Mn$_{0.8}$Co$_{0.2}$, however, the diffuse scattering intensity decreases with increasing temperature, and almost disappears at $T = 200$ K 21. Therefore, the SRO transition temperature may be approximately 200 K for $\beta$-Mn$_{0.8}$Co$_{0.2}$. These results suggest that the SRO transition temperature rapidly decreases toward the quantum critical point, as illustrated in Fig. 6. Near the critical point, the family of $\beta$-Mn compounds exhibits NFL behavior 22, as observed in MnSi 24. Therefore, the phase diagram of Fig. 6 may include B20 family compounds. The SRO of MnSi at ambient pressure occurs at 1 K above the helical magnetic order temperature of 29 K 24. For FeGe, the precursor region corresponds to ~2 K above the long-range magnetic order temperature of 278.2 K 5, and the NFL behavior seems to disappear in the SG/AFM phase. Thus far, the SRO has a limited temperature range, possibly because of the weak DM interaction of 3$d$ elements. The pseudogap state of cuprates may also be categorized as an unconventional magnetic ordered state of conduction electrons 27. This issue is a central concept in condensed matter physics.
accompanied by Fermi surface reconstruction. The magnetic ordering of cuprates is suppressed by their low-dimensionality in addition to carrier doping, whereas the large superexchange coupling $J$ leads to the development of unconventional magnetic order as the pseudogap state. In contrast, the magnetic ordering of Mn$_3$RhSi with a large Mn magnetic moment is suppressed by geometrical frustration, where SRO appears at high temperatures. Here, the present finding of SRO in Mn$_3$RhSi provides a novel platform for studying the unique properties of unconventional magnetic order over a wide temperature range.

**Methods**

**Sample preparation and quality.** Polycrystalline samples were prepared from stoichiometric amounts of high-purity powders of the constituent elements (99.9% pure Mn, 99.9% pure Rh, and 99.9% pure Si). The compounds were synthesized by a conventional arc melting method in an argon atmosphere. The polycrystals were sealed in an evacuated quartz tube, annealed at 900 °C for 3 days and 800 °C for 1 week, and subsequently quenched in water. The phase purity was examined by a conventional arc melting method in an argon atmosphere. The polycrystals were sealed in an evacuated quartz tube, annealed at 900 °C for 3 days and 800 °C for 1 week, and subsequently quenched in water. The phase purity was examined by X-ray powder diffraction using a desktop diffractometer with Cu Ka radiation. No traces of impurity phases were found within the experimental accuracy. The chemical composition of the samples was verified by scanning electron microscopy and energy-dispersive X-ray spectroscopy (SEM/EDS) analysis. The SEM/EDS elemental mapping indicated a homogeneous distribution of atoms and an atomic ratio of Mn:Rh:Si = 58:21:22, which is consistent with the stoichiometric composition within an error of ±1%. Magnetization measurements were performed using a Superconducting Quantum Interference Device magnetometer at the CROSS-Tokai User Laboratory II. Specific heat measurements were performed with an AC capacitance bridge in a two-probe configuration.

**Neutron diffraction experiments.** Neutron powder diffraction data were collected on the Wide-Angle Neutron Diffractometer (WAND, IB-2C) at the HFIR Isotope Reactor (HFIR) at Oak Ridge National Laboratory (ORNL), employing Ge (113) reflection to produce a monochromatic neutron beam with a wavelength of 1.4827 Å. A 5.0 g powder sample was loaded into a vanadium can (7.5-mm inner diameter). Crystal and magnetic structure refinements were performed by the Rietveld method with the program FullProf$^2$ and visualized with the software VESTA$^2$. The magnetic form factor of the Mn atom was used in the analysis. Representational analysis was conducted using the program SARA$^2$ to identify a reasonable model for the symmetry-allowed magnetic structure.

The absolute magnetic diffuse scattering intensity was estimated using the method described in Supplementary Note 4, and the results were analyzed following the method described in Supplementary Note 5.

**Muon spin relaxation measurements.** The μSR experiments were performed using the HiFi and ARGUS spectrometers at the ISIS facility, Rutherford Appleton Laboratory. A polycrystalline ingot was cut and mounted in a light furnace for high-temperature measurements. The decay-position asymmetry function was measured as a function of time, under zero field or under a longitudinal field of 10 mT, as shown in Supplementary Note 5. The volume fraction shown in Fig. 3b was estimated from the normalized asymmetry as follows. The initial asymmetry is an instrumental parameter that can be obtained from a non-magnetic material, such as a silver foil. The asymmetry decreases in a magnetically ordered material over a short time, depending on the magnetic moment size. The decreasing time can be very short, on the order of 0.2 μs. In this case, the asymmetry can be observed as a sudden reduction near the zero time point using a pulsed muon spectrometer. The magnitude of the reduction in the spectrum is the ratio of the magnetically ordered volume because the muons randomly exhibit local magnetic ordering. The zero position of the zero magnetic moment was determined from the maximum initial asymmetry of the original time spectra at 700 K, which had a value of 20.8%. Therefore, in the normalized asymmetry graph, a value of 1 corresponds to the initial asymmetry of the time spectra at 700 K, and 0 indicates the minimum asymmetry of the time spectra at 300 K for up to 15 μs, considering the lower limit of the error bar. The minimum asymmetry was 14.1% in this case. The same approach was applied to normalize the time spectrum acquired at 320 K from a different spectrometer, which confirmed the reproducibility of the data and analysis. It should be noted that the magnetic volume consists of the quasistatic magnetic moments in μSR time window below 0.1 meV.

**Data availability**

All relevant data are available from the authors on request.

**Code availability**

The program FullProf is distributed free of charge (https://www.ill.eu/sites/fullprof/). The software VESTA is distributed free of charge for academic users under the VESTA License (https://jp-minerals.org/ves/vesa/p/download.htm).

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