Switched Reluctance Motors (SRMs) offer numerous advantages over DC or AC drives due to their mechanical simplicity, efficiency, low cost, and robust construction (Miller, 1993; Katalenic, 2013), see Figure 1. Its application is particularly attractive when maintenance is expensive or the costs should be low, e.g., in optical communication terminals on satellites (Kramer et al., 2020). On the other hand, a main drawback of SRMs is the complexity in controlling its position, due to the nonlinear relationship between torque, rotor angle, and currents to the different phases. These nonlinear dynamics are typically attempted to be linearized using a commutation strategy (Wang, 2016), as shown in Figure 2, and if done imperfectly, this will introduce a torque ripple to the rotor.

The problem of finding a commutation strategy is inherently over-parametrized, since at any rotor position, multiple coils can apply a torque to the rotor. Model-based methods of designing a commutation strategy assume that a description of the nonlinear relation between torque, current and rotor angle is available, and define a torque sharing function to divide the currents over the coils (Balaji et al., 2004; Ilić-Spong et al., 1987). The specification of this torque sharing function is often done in an ad-hoc manner (Wang, 2016; Vujicic, 2012), and experimental validation is required to determine which function leads to the least torque ripple, since each function is a valid solution of the over-parametrized commutation problem.

In a different line of developments, non-parametric modeling has attracted increased attention in the last decades due to its flexible model structures. In particular, Gaussian Process (GP) regression (Rasmussen and Williams, 2006) has been applied extensively to motion control (Poot et al., 2022), since it admits intuitive model structures based on properties such as smoothness and periodicity, and allows for automatic optimization of hyper-parameters to fit a continuous function through a finite number of points. Although conventional model-based design methods for commutation strategies lead to a highly flexible control scheme that allows for the use of linear controllers, current design techniques of commutation functions do not take a major cause of torque ripple into account. In fact, this paper shows that even if a perfect model is available, torque ripple still occurs because of sampling effects. If the sampling rate is decreased or the velocity is increased, this sampling-induced torque ripple increases. Indeed, low-cost applications that would benefit from the simplicity of SRMs may not allow for high sampling rates.

Therefore, the aim of this paper is to reduce sampling-induced torque ripple in the presence of a perfect model, by formulating a commutation function that divides currents between coils specifically to reduce sampling-induced torque ripple. To this end, an optimization problem is posed that penalizes torque ripple and power consumption as a function of the commutation function. The problem is solved to find realizations of an optimal commutation strategy that allows for the use of linear controllers, current and rotor angle is available, and define a torque sharing function to divide the currents over the coils (Balaji et al., 2004; Ilić-Spong et al., 1987). The specification of this torque sharing function is often done in an ad-hoc manner (Wang, 2016; Vujicic, 2012), and experimental validation is required to determine which function leads to the least torque ripple, since each function is a valid solution of the over-parametrized commutation problem.

In a different line of developments, non-parametric modeling has attracted increased attention in the last decades due to its flexible model structures. In particular, Gaussian Process (GP) regression (Rasmussen and Williams, 2006) has been applied extensively to motion control (Poot et al., 2022), since it admits intuitive model structures based on properties such as smoothness and periodicity, and allows for automatic optimization of hyper-parameters to fit a continuous function through a finite number of points. Although conventional model-based design methods for commutation strategies lead to a highly flexible control scheme that allows for the use of linear controllers, current design techniques of commutation functions do not take a major cause of torque ripple into account. In fact, this paper shows that even if a perfect model is available, torque ripple still occurs because of sampling effects. If the sampling rate is decreased or the velocity is increased, this sampling-induced torque ripple increases. Indeed, low-cost applications that would benefit from the simplicity of SRMs may not allow for high sampling rates.

Therefore, the aim of this paper is to reduce sampling-induced torque ripple in the presence of a perfect model, by formulating a commutation function that divides currents between coils specifically to reduce sampling-induced torque ripple. To this end, an optimization problem is posed that penalizes torque ripple and power consumption as a function of the commutation function. The problem is solved to find realizations of an optimal commutation function at a finite number of motor angles. Subsequently, a prior is posed on the commutation function, based on smoothness and periodicity, and Gaussian Process regression is used to obtain a continuous commutation function. The resulting function is fundamentally different from conventional commutation functions, and closed-loop simulations show significant reduction of the error. The results offer a new perspective on suitable commutation functions for accurate control of reluctance motors.

### Keywords
Switched Reluctance Motor, Linearization, Feedback Control, Nonparametric methods, Static optimization problems, Convex optimization.
This paper is structured as follows. In Section 2, the setting and commutation strategy are given, and it is explained how sampling can introduce torque ripple. Subsequently, Section 3 describes the developed design method for a commutation strategy that reduces sampling-induced torque ripple. Next, Section 4 describes the simulation results, and finally, 5 presents the conclusion, as well as directions for further research.

2. PROBLEM DESCRIPTION

In this section, the problem description is given. First, the working principle of a switched reluctance motor is explained, which serves as the motivating example for the research in this paper. Next, the system and the commutation strategy are described. Subsequently, it is shown that torque ripple appears even in the presence of a perfect model, because of sampling effects. Finally, the problem formulation is given.

2.1 Switched reluctance motor concept

The SRM, depicted schematically in Figure 1, consists of a rotor with \( n \) teeth, positioned between three coils (Kramer et al., 2020). Each coil \( c \in \{1, 2, 3\} \) can be magnetized separately by application of a current \( i_c(t) \in \mathbb{R} \) at time \( t \in \mathbb{R} \). Neglecting magnetic saturation, the resulting torque on the rotor is given (Miller, 1993) by

\[
T_c(\phi, i_c) = \frac{1}{2} \frac{dL_c(\phi)}{d\phi} i_c^2, \tag{1}
\]

where \( L_c(\phi) \) is the phase inductance as a function of rotor position \( \phi \). The inductance is maximal when the rotor teeth are aligned with the teeth that are magnetized by the coil, and minimal when these do not overlap. Hence, \( L_c(\phi) \) is periodic in \( \phi \) with spatial period \( \frac{2\pi}{n_t} \). Since the required current to generate a torque depends on \( \phi \) in (1), a commutation strategy is desired that divides currents between the coils based on \( \phi \) to achieve some desired torque. This is explained in detail in the next section.

2.2 Setting and goal

First, the nonlinear dynamics of the switched reluctance motor are defined. The multi-input single-output (MISO) system is given by

\[
T(k) = g(\phi(t), u(t))
\]

with \( A \in \mathbb{R}^{n \times n}, B \in \mathbb{R}^{n \times 1}, C \in \mathbb{R}^{1 \times n} \). The output \( \phi(t) \in \mathbb{R} \) denotes position in radians and the input \( u(t) \in \mathbb{R} \) is a vector of squared currents, i.e., \( u := [i_1^2, i_2^2, i_3^2] \top \). The function \( g : \mathbb{R} \times \mathbb{R}^3 \mapsto \mathbb{R} \) is defined as

\[
g(\phi, u) := [g_1(\phi) \ g_2(\phi) \ g_3(\phi)] u, \tag{3}
\]

where each \( g_c(\phi) : \mathbb{R} \mapsto \mathbb{R} \) is a periodic function with spatial period \( p = \frac{2\pi}{n_t} \), see Figure 3 for an example. For ease of notation, \( g(\phi, u) \equiv g(\phi) u \). Moreover, \( g \) is assumed to be known.

At intervals of \( T_s \) seconds, the rotor position is sampled by the ideal sampler \( S \), defined as

\[
S : \phi(k) = \phi(kT_s), \quad k \in \{0, 1, \ldots\}. \tag{4}
\]

Furthermore, the ideal zero-order-hold \( \mathcal{H} \) is used to interpolate the input \( u(k) \) between samples, i.e.,

\[
\mathcal{H} : u(kT_s + \delta) = u(kT_s), \quad \delta \in [0, T_s).
\]

The aim is to construct a commutation function \( f : \mathbb{R} \times \mathbb{R} \mapsto \mathbb{R}^3 \geq 0 \) that linearizes \( g(\phi) \), i.e.,

\[
T = g(\phi) f(\phi, T^*) = T^*, \tag{6}
\]

see Figure 2. If (6) holds, \( T^* \) can be considered to be the input to the linear system \( G \) described by state-space matrices \((A, B, C)\), and linear feedback control can be used, see Figure 4.

2.3 Torque ripple due to sampled data aspects

In practice, torque ripple will always occur on a switched reluctance motor, because the commutation function can only linearize the nonlinear function \( g \) on the samples, but not in between samples. This is explained as follows.

![Fig. 1. Schematic overview of the Switched Reluctance Motor. By sequentially applying current waveforms to the coils, a torque is applied to the toothed rotor.](image1)

![Fig. 2. Overview of the commutation strategy.](image2)

![Fig. 3. Example function \( g(\phi_n) \). The torque-current relationship is clearly periodic in the rotor angle, and it slightly differs for each of the three coils.](image3)
The function $g$ would be perfectly linearized if (6) holds at all times, i.e.,
$$T(t) = g(\phi(t))f(\phi(t))T^*(t) = T^*(t), \quad \forall t.$$ (8)
This equation cannot be satisfied in practice, because the zero-order-hold scheme in (5) leads to
$$T(kT_s + \delta) = g(\phi(kT_s + \delta))f(\phi(kT_s))T^*(kT_s),$$ with $\delta \in (0, T_s)$. The produced torque $T(kT_s + \delta)$ does not equal $T^*(kT_s + \delta)$ in general, since
$$g(\phi(kT_s + \delta))f(\phi(kT_s)) \neq 1,$$ (10)
and therefore, a torque ripple occurs between samples, i.e., $T(t) \neq T^*(t)$ for $t \neq kT_s$. The absolute torque ripple is defined as
$$e_T(t) = T(t) - T^*(t),$$ (11)
and the relative torque ripple as
$$e_{T,rel}(t) := \frac{e_T(t)}{T^*(t)}.$$ (12)
In between samples $k$ and $k+1$, i.e., at times $\tau \in [kT_s, (k+1)T_s)$, the relative torque ripple can be written as
$$e_{T,rel}(\tau) := \frac{T(\tau) - T^*(kT_s)}{T^*(kT_s)},$$ (13)
so the relative torque error for any given time $t$ is given by
$$e_{T,rel}(t) = e_{T,rel}^{(k)}(t) = g(\phi(t))f(\phi(kT_s)) - 1,$$ (14)
where $\lfloor \cdot \rfloor$ denotes the floor operator.

The convolution of the absolute torque ripple with the continuous-time system $G$ will result in a ripple in $\phi(t)$, which may be nonzero on the samples. Consequently, in closed-loop, a periodic position error will occur because of sampling-induced torque ripple.

### 2.4 Problem formulation

The above analysis motivates the necessity of taking sampling effects explicitly into account when constructing commutation functions. As such, the aim of this paper is to construct a commutation function $f$, with the structure defined in (7), that satisfies the following requirements:

R1: The nonlinear function $g$ must be linearized on the samples, i.e.,
$$g(\phi(kT_s))f(\phi(kT_s)) = 1.$$ (15)

R2: The 2-norm of the relative torque ripple, i.e., $\|e_{T,rel}\|_2$ is as small as possible, see (14). Note that $\|e_{T,rel}\|_2$ will always be greater than zero for $T_s > 0$.

R3: The power consumption of the commutation strategy during constant velocity, given by
$$E[f] = \sum_c \|f_c(\phi)\|_1,$$ (16)
is as small as possible.

In the next section, it is explained how this problem is solved.

### 3. OPTIMAL COMMUTATION

In this section, it is explained how a commutation function can be constructed that minimizes both sampling-induced torque ripple and power consumption. The key idea is to pose a finite-dimensional optimization problem that explicitly takes R1, R2 and R3 into account, to obtain realizations of an optimal commutation function at a number of rotor angles. Since a commutation function must be continuous, the finite-dimensional solution is used to pose a regression problem, in order to fit a function with some specific structure. In particular, Gaussian Process regression is used.

First, the optimization problem that addresses the problem posed in Section 2.4 is defined. Subsequently, it is explained how Gaussian Process regression yields a continuous commutation function with a specific model structure. Finally, it is explained how the hyper-parameters of this model can be found automatically.

#### 3.1 Optimization problem

The requirements R1, R2, and R3 posed in Section 2.4 are used to form an optimization problem as follows. The design variables are defined as
$$F := [f(\phi_{m,1}), ..., f(\phi_{m,N})]^\top,$$ (17)
where the relative motor angles $\phi_{m}$ are defined as
$$\phi_{m} := \phi - 2\pi \left[ \phi + \frac{\pi}{2\pi} \right],$$ (18)
and $\phi_{m,i}$ are chosen to be regularly spaced between $-\pi$ and $\pi$. Moreover, a nominal velocity is defined as
$$v = \frac{2\pi}{n_4NT_s},$$ (19)
such that when moving at $v$ rad/s, every time $t = kT_s$ corresponds with a relative position $\phi_m(t) = \phi_{m,k}$. At this velocity, samples in time are aligned with the design variables.

It then follows that R1, see (15), can be written as $N$ equality constraints that are linear in the design variables, namely,
$$g(\phi_{m,i})f(\phi_{m,i}) = 1, \quad \forall i \in [1, ..., N].$$ (20)
Moreover, it must hold that
$$f(\phi_{m,i}) \geq 0, \quad \forall i \in [1, ..., N].$$ (21)

Next, the cost function of the optimization problem is defined, which includes both R2 and R3. The 2-norm of the relative torque ripple (14) is approximated numerically by dividing each sample into $M$ sub-samples to construct
$$e_{T,rel}(t) = e_{T,rel}(0), ..., e_{T,rel}\left(NT_s - \frac{T_s}{M}\right), e_{T,rel}(NT_s)^\top,$$ (22)
which is linear in the design variables. Finally, R3 is satisfied by including $\|F\|_1$ in the cost function, which is defined as
$$\|F\|_1 := \sum_c \|f_c(\phi_{m,1}), ..., f_c(\phi_{m,N})\|^\top_1.$$ (23)
This leads to the following convex optimization problem.
$$\min_{F} \|F\|_1 + \beta \|e_{T,rel}\|_2,$$ (24)
subject to (17), (20), (21), where $\beta \in \mathbb{R}_{>0}$ is a constant that acts as a trade-off between low power consumption and low torque ripple.
Remark 1. Other terms that enforce desired properties on \( f \) can be easily added to the cost function, e.g., \( \| F \|_{\mathcal{M}} \), where \( \mathcal{M} \) defines a norm that enforces smoothness of \( f \), or \( \| F \|_{\infty} \), such that peak currents are minimized.

It is shown next how a continuous commutation function \( f \) is created from a finite number of optimal values \( F^* \).

### 3.2 Obtaining a commutation function with Gaussian Process regression

A commutation function must be continuous, i.e., it must yield squared currents for any rotor angle and requested torque. Since the solution to optimization problem (24) contains only \( N \) realizations of the optimal commutation function, interpolation is required. The underlying structure of the optimal commutation function is unknown, other than it being periodic in \( \phi \). Therefore, a structure is chosen that can represent a large range of functions, based on the smoothness and periodicity of \( f \), as follows.

The commutation functions \( f_c \) of the coils \( c \in [1, 2, 3] \) are assumed to be of the form

\[
f_c(\phi^*_m) = \sum_{i=1}^{N} \alpha_i k_c(\phi^*_m, \phi_{m,i}) = k_c(\phi^*_m, \Phi_m) \alpha_c, \tag{25}
\]

where \( \phi^*_m \) denotes an arbitrary relative position, \( \phi_{m,i} \) are as defined in the previous section, \( \alpha \in \mathbb{R}^N \) is a vector of weights and

\[
k_c(\phi^*_m, \Phi_m) := [k_c(\phi^*_m, \phi_{m,1}), \ldots, k_c(\phi^*_m, \phi_{m,N})]. \tag{26}
\]

The kernel function \( k_c(\phi_{m,i}, \phi_{m,j}) \) imposes some nonlinear structure on \( f \), as explained in detail in Section 3.3.

The regression problem is then posed as follows. Given a kernel function \( k_c \), the weights \( \alpha_c \) that best fit the observations \( F^* \) of \( f^*(\phi^*_m) \) are obtained by solving the following GP regression problem for each \( c \in [1, 2, 3] \):

\[
\min_{\alpha_c} J[f_c] = \| F^*_c - K_c \alpha_c \|^2 + \sigma^2_{c,n} \alpha_c^T K_c \alpha_c, \tag{27}
\]

where \( K_c \) is shorthand for the Gramian \( K_c(\Phi_m, \Phi_m) \) and \( \sigma^2_{c,n} > 0 \) is the regularization strength. This problem has the solution

\[
\alpha_c = (K_c + \sigma^2_{c,n} I)^{-1} F^*_c, \tag{28}
\]

and hence, the continuous commutation function \( f_c \), which is defined for an arbitrary \( \phi^*_m \) is given by

\[
f_c(\phi^*_m) = k_c(\phi^*_m, \Phi_m) \alpha_c. \tag{29}
\]

The next section explains the choice of kernel function \( k_c \).

### 3.3 Kernel function

From (25), it is clear that the kernel function \( k_c \) imposes structure, or a prior, on the function space of \( f_c \). A convenient choice that allows for a large degree of flexibility is to pose a prior on the degree of smoothness of \( f_c \), this is done with a Matérn kernel (Rasmussen and Williams, 2006) of the form

\[
k_{c, \mu/2}(x, x') = \sigma^2_0 \exp\left(-\sqrt{2\mu + 1} \rho^2 \right) \frac{\mu!}{(2\mu)!} \rho^\mu \sum_{i=0}^{\mu} \frac{(\mu + i)!}{\mu! (\mu - i)!} \left(2\sqrt{2\mu + 1} \rho \right)^{\mu - i}, \tag{30}
\]

where \( \mu \in \mathbb{N} \), and \( \rho = \sqrt{(x - x')^2 / L^2} \). A function \( f_c(\phi^*_m) \) parametrized by this kernel through (29) is \( \mu \)-times differentiable in the mean-square sense, and hence, the parameter \( \mu \) relates to the smoothness of \( f_c \). Moreover, it is known that the commutation function is periodic in \( \phi \) with spatial period \( p = \frac{\pi}{n_t} \), and this periodicity is enforced on \( f_c \) by \( k_c \) by defining

\[
x = \begin{bmatrix} \sin \frac{2\pi \phi_m}{p} \\ \cos \frac{2\pi \phi_m}{p} \end{bmatrix}, \quad x' = \begin{bmatrix} \sin \frac{2\pi \phi_m'}{p} \\ \cos \frac{2\pi \phi_m'}{p} \end{bmatrix}, \tag{31}
\]

see (Duvenaud, 2014, Section 2.7) for further details. The parameters \( \mu, \ell, \sigma^2_0 \) and \( \sigma^2_{n,c} \) can be tuned automatically, as is explained next.

### 3.4 Optimization of hyper-parameters

The model structure of the commutation function in (29) is a function of the kernel, and hence, it depends on the kernel hyper-parameters \( \Theta := \{\mu, \ell, \sigma^2_0, \sigma^2_{n,c} \} \). To find a model structure of \( f_c \) that is most consistent with the realizations \( F^*_c \) following from (24), the marginal likelihood is maximized. The marginal likelihood \( p(F^*_c | \Phi_m, \Theta) \) is the probability of the data given the model, parametrized by (30) in terms of \( \Theta \). Its logarithm is given by

\[
\log p(F^*_c | \Phi_m, \Theta) = -\frac{1}{2} (F^*_c)^T (K_c(\Theta))^{-1} F^*_c - \frac{1}{2} \log \det(K_c(\Theta)) - N \log 2\pi,
\]

with \( K_c(\Theta) = K_c + \sigma^2_{n,c} I \). By maximizing this expression with respect to \( \Theta \), the hyper-parameters \( \Theta^* \) are found such that commutation function \( f_c(\phi^*_m, \Theta^*) \) in (29) is the most likely fit through \( F^*_c \) given the kernel structure.

### 4. SIMULATION RESULTS

The method is applied to a simulation example to demonstrate its effectiveness in reducing torque ripple. The setting is explained first, after which the results are presented.

#### 4.1 Setting

Consider the control scheme in Figure 2. The system, consisting of a mass and a damper, is described by

\[
G(s) = \frac{1}{8(s + 1)^5},
\]

and the controller, with sampling rate \( F_s = 1000 \text{ Hz} \), by

\[
C(z) = \frac{6.72 \cdot 10^{-5} z^2 - 1.1 \cdot 10^6 z + 4.51 \cdot 10^5}{z^2 + 1.03z + 0.0296},
\]

such that the bandwidth is 100 Hz. The function \( q \) is shown in Figure 3, where the torque-current relationship is deliberately defined differently for every coil, see also Kramer et al. (2020). The rotor of the SRM consists of \( n_t = 131 \) teeth. The goal is to track a number of second-order references which consist of a constant acceleration part during 5 teeth, and a constant velocity part during 15 teeth, where \( v_j \) is different for every reference.

#### 4.2 Approach

The optimization problem (24) is posed at \( N = 150 \) points with \( M = 15 \) subsamples per sample. The parameter \( \beta \) that trades off power consumption and sampling-induced torque ripple is chosen as \( \beta = 1000 \), and (24) is solved with SeDuMi, see Sturm (1999). Subsequently, for every coil a kernel in the form of (30) is defined with \( \mu = 3 \) and \( p = \frac{\pi}{n_t} \).

The parameters \( \ell, \sigma^2_0 \) and \( \sigma^2_{n,c} \) are found by maximization...
Clearly, \( f \) is periodic in \( \phi_m \) and it is fitted well through \( F^* \). The commutation function is different for every coil because \( g_c \) is different for every coil.

Since \( |f^*| \) is always small, since then \( g(c) = 1 \), it does not hold that \( g(\phi_m) f(\phi_m) = 1 \), i.e., R1 is not satisfied in general by commutation functions based on torque sharing. To prevent the need for saturation as much as possible, the overlap is typically chosen to be small, since then \( f(\phi_m) = 0 \) at positions where \( g(\phi_m) \approx 0 \). In this example, the overlap between the commutation functions is chosen to be \( \phi_{m,ov} \approx \frac{\pi}{4} \) radians, and the saturation level is chosen to be \( a = 3 \frac{\text{A}}{\text{Nm}} \).

In contrast to conventional commutation functions, the optimal commutation function is not constructed through piece-wise division by \( g_c(\phi_m), c \in [1, 2, 3] \) as in (35), and hence, a large degree of overlap can be achieved while still satisfying R1.

Next, the closed-loop performance of \( f^* \) is compared to conventional approaches, see Figure 7. The position error is reduced significantly for a range of velocities. At low velocities, the effect of torque ripple is negligible, since \( \phi_m(\tau) \approx \phi_m(kT_s) \) for a given \( T_s \), and hence \( e_{r,T_{rel}}(\tau) \) is small in (13). This is confirmed by the results in Figure 7. Consequently, the performance increase is most pronounced at higher velocities.
4.4 Torque ripple vs. energy consumption

A tuning knob in the developed approach is $\beta$, which trades off power consumption and torque ripple in (24). Figure 10 compares some commutation functions for different values of $\beta$. As expected, it can be seen that a larger emphasis on power consumption, corresponding to a small $\beta$, yields commutation functions with a smaller area.

Moreover, Figure 11 shows the performance increase with respect to $f_{\text{sine}}$, for different values of $\beta$ at $v = 8$ teeth/s. As expected from (24), the torque ripple is reduced most for large values of $\beta$ and consequently, the reduction in the position error is most pronounced, at the cost of increased energy usage. Note that the energy consumption is evaluated in closed-loop, and thus, if low values of $\beta$ lead to large errors, the feedback controller will lead to more energy consumption as well.

From these results it is clear that by optimizing a commutation function explicitly to reduce inter-sample torque ripple, a function is obtained that is fundamentally different from conventional commutation functions, leading to significantly better performance in closed-loop. The parameter $\beta$, that trades of power consumption and torque ripple, is an intuitive tuning knob of the approach. This parameter is shown to influence the degree of overlap in currents between different coils, which is in contrast with conventional approaches, where the degree of overlap is chosen in an ad-hoc manner. The results offer a new perspective on solutions to the over-parametrized commutation problem, and suggest that the developed approach is arguably more methodical and intuitive than conventional approaches based on torque sharing functions.

5. CONCLUSION AND FUTURE WORK

In this paper, it is shown that sampling effects are a cause of torque ripple in switched reluctance motors, and that this ripple can be significantly reduced by exploiting the design freedom inherent in the commutation problem. The resulting commutation functions are fundamentally different from conventional functions found in literature, leading to a factor 45 decrease in the 2-norm of the error in simulation. The performance increase is especially pronounced at high velocities or low sampling rates.

As in most commutation strategies, the design of the commutation function relies on a model of the nonlinear relationship $g$ between torque, current and angle. Since the developed approach exploits knowledge of $g$ in the optimization problem, the effectiveness in practice depends on the model quality. Therefore, future work will be aimed towards data-driven design of commutation functions.

REFERENCES

Balaji, M., Vaitilingam, C.A., and Kamaraj, V. (2004). Torque ripple minimization in switched reluctance motor drives. IEEE Conference Publication, 1(1), 104–107.

Duvenaud, D. (2014). Automatic model construction with Gaussian processes. Ph.D. thesis, University of Cambridge.

Ilić-Spong, M., Miller, T.J., Macminn, S.R., and Thorp, J.S. (1987). Instantaneous Torque Control of Electric Motor Drives. IEEE Transactions on Power Electronics, PE-2(1), 55–61.

Katalenic, A. (2013). Control of reluctance actuators for high-precision positioning. Ph.D. thesis, Eindhoven University of Technology.

Kramer, L., Peters, J., Voorhoeve, R., Witvoet, G., and Kuiper, S. (2020). Novel motorization axis for a Coarse Pointing Assembly in Optical Communication Systems. In IFAC PapersOnLine, volume 53, 8426–8431. Elsevier Ltd.

Miller, T.J.E. (1993). Switched Reluctance Motors and Their Control, volume 31. Oxford University Press, London, England.

Poot, M., Portegies, J., Moorren, N., van Haren, M., van Meer, M., and Oomen, T. (2022). Gaussian Processes for Advanced Motion Control. IEEE Journal of Industry Applications, 21011492.

Rasmussen, C. and Williams, C. (2006). Gaussian processes for machine learning. London, England.

Sturm, J.F. (1999). Using SDuMi 1.02, a MATLAB toolbox for optimization over symmetric cones. Optimization methods and software, 11(1-4), 625—653.

Vujicic, V.P. (2012). Minimization of Torque Ripple and Copper Losses in Switched Reluctance Drive. IEEE Transactions on Power Electronics, 27(1), 388–399.

Wang, J.J. (2016). A common sharing method for current and flux-linkage control of switched reluctance motor. Electric Power Systems Research, 131, 19–30.