Combining LoRaWAN and a New 3D Motion Model for Remote UAV Tracking

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Abstract—Over the last few years, the many uses of Unmanned Aerial Vehicles (UAVs) have captured the interest of both the scientific and the industrial communities. A typical scenario consists of the use of UAVs for surveillance or target-search missions over a wide geographical area. In this case, it is fundamental for the command center to accurately estimate and track the trajectories of the UAVs by exploiting their periodic state reports. In this work, we design an ad hoc tracking system that exploits the Long Range Wide Area Network (LoRaWAN) standard for communication and an extended version of the Constant Turn Rate and Acceleration (CTRA) motion model to predict drone movements in a 3D environment. Simulation results on a publicly available dataset show that our system can reliably estimate the position and trajectory of a UAV significantly outperforming baseline tracking approaches.

I. INTRODUCTION

Over the last few years, Unmanned Aerial Vehicles (UAVs) have entered the mainstream: the commercialization of low-cost drones for amateur and professional use is quickly increasing the number of flying units, which will soon be measured in millions, according to the U.S. Federal Aviation Administration (FAA) [1]. Their integration in cellular networks, both as end-users and as coverage extenders [1], is already being discussed, and 5G systems are expected to make use of UAVs of different sizes, from small-scale low-altitude drones to communication satellites [2]. Although energy and battery concerns are still critical [3], the use of UAVs is being proposed for several kinds of scenarios, from remote infrastructure monitoring [4] to disaster monitoring [5] and relief [6].

As the capabilities of UAVs evolve towards the full support of safety-critical applications, accurate positioning of drones is going to become more and more important. Although UAVs often have on-board Global Positioning System (GPS) receivers, filtering [7] and data fusion techniques, often integrating camera image processing [8], can significantly improve the positioning accuracy by combining several measurements into a single solution that is more robust and precise than any individual approach.

In this work, we propose a system to remotely track the position of a UAV moving in a 3D environment. In the considered scenario, a mission control station exploits a novel 3D motion model, called 3-Dimensional CTRA (3D-CTRA), to follow the trajectory of the target. Our model extends the well-known Constant Turn Rate and Acceleration (CTRA) model, widely used in vehicular scenarios, by adding a third dimension which allows it to represent even complex banking maneuvers accurately. We also study a simpler model, named CTRA+, which considers linear motion on the vertical axis. In both cases, the tracking mechanism is the same: the UAV periodically transmits its state, including the heading, speed and acceleration, and the control station estimates the target position by evolving the motion model. In this way, even sporadic updates allows the system to accurately track the UAV.

In our system, state updates are transmitted through the LoRaWAN communication standard. This technology allows the transmission of low-bitrate messages at very long distances, enabling the control station to track the drone at ranges of several kilometers with minimal infrastructure. Considering the limited duty cycle imposed by the LoRaWAN specifications, our system can support swarms of up to 72 drones with a packet collision rate below 10% by using different Spreading Factors (SFs) [9]. When LoRaWAN is tuned to achieve larger communication range, the intervals between transmissions can last several seconds, thus making the tracking more difficult. It is hence interesting to analyze the feasibility of such a framework, and to investigate its performance when varying the considered mobility model. We tested our system in extensive ns-3 simulations using the UAV mobility traces from the Mid-Air public dataset and comparing the two mobility models we proposed against a baseline solution implementing Dead Reckoning (DR), a well-known tracking method exploiting a uniform rectilinear motion model to predict the target movements. The results show that the more accurate 3D-CTRA mobility model can bring an improvement of up to 30% on the 75th percentile tracking error.

The rest of the paper is organized as follows. Sec. II presents the state of the art on UAV applications and tracking models, including both GPS and visual data. Sec. III presents the CTRA+ and 3D-CTRA models, including the relative update equations, and describes the LoRaWAN standard and the frequency plan needed for our application. The simulation settings and the results are described in Sec. IV while Sec. V presents our concluding remarks and ideas for future work.

II. RELATED WORK

UAVs popularity has grown exponentially over the past few years, and their widespread use could enable a real Internet of Flying Robots [10] in the near future. Drones are used
for environmental monitoring in a wide range of scenarios, from traffic jam detection \cite{11} to industry and agriculture \cite{12}, and are poised to become a key Smart City infrastructure \cite{13}. UAVs are also being used in combination with ground-based robots to help them perform complex tasks \cite{14}. However, disaster management and relief is perhaps the most interesting application for UAVs; drones can easily avoid ground-level obstacles and flooded areas by flying over them, surveying the extent of the damage \cite{5} or helping with search and rescue operations \cite{6} and communications. In order to enable these critical services, controllers must be able to follow and anticipate the drone’s trajectory. This requires the UAV to transmit frequent positioning updates \cite{15}, often at long ranges.

The target tracking problem is a well-studied research topic, and is usually solved by representing the target’s motion using simple models and estimating its position with a Bayesian Filtering (BF) algorithm. The best-known BF algorithms used in this context are the Kalman Filter (KF) \cite{10} and the Particle Filter (PF) \cite{17}. Long-term forecasting can be achieved by simply applying the predictive step of the BF to the last available state estimation. However, this solution does not provide good performance when updates are infrequent, especially if the model is inaccurate. In this perspective, our work tries to minimize broadcasting operations while ensuring accurate position estimation.

The tracking problem has been widely explored in 2D vehicular scenarios \cite{18}, often using the CTRA model \cite{19}, which considers an accelerating vehicle with constant turn rate. A similar model for drones moving horizontally was presented in \cite{20}, including Gaussian noise on the motion parameters. A more complex model with several possible maneuvers was described in \cite{21}, adapting the CTRA settings to draw the correct trajectory. In general, motion models for drones are based on 2D CTRA or simpler models with constant speed \cite{22} or heading \cite{23}. To the best of our knowledge, our CTRA+ and 3D-CTRA models are the first models that can represent 3D maneuvers with the same flexibility that CTRA has in the 2D space.

III. System Model

In this work, we model a UAV which periodically transmits its state to a control station using the LoRaWAN communication standard. The aim of the control station is to accurately track the UAV position in different scenarios. To represent the drone motion in a 3D environment, we consider three possible models, i.e., DR, CTRA+, and 3D-CTRA. In the rest of the section, we first extend conventional CTRA, obtaining the system equations for CTRA+ and 3D-CTRA. Then, we analyze the tracking and communication frameworks.

A. The CTRA+ model

While standard CTRA only tracks the yaw, i.e., the angle $\theta$ between the drone’s heading and the reference direction on the horizontal plane, 3D motion models must also consider the pitch, i.e., the vertical angle $\phi$ between the drone’s heading and the horizon. Moreover, the target state must include the altitude $z$ as well as the horizontal position $(x, y)$, resulting in the 5-tuple $(x, y, z, \theta, \phi)$. These parameters are common to all the motion models we implement. However, none of our models explicitly considers roll, which is not strictly necessary to represent motion in a 3D space.

In 2D CTRA, the turn rate $\omega = \frac{d\phi}{dt}$ is assumed to be constant. The CTRA+ model makes the same assumption and, moreover, considers a constant pitch $\phi$:

$$\theta(t) = \theta(0) + \omega t \quad (1)$$
$$\phi(t) = \phi(0) \quad (2)$$

where $\theta(0)$ and $\phi(0)$ represent the initial heading of the drone.

Like standard CTRA, CTRA+ assumes the tangential acceleration $a = \frac{dv}{dt}$ to be constant, which turns the circular motions into Archimedean spirals \cite{24}. In particular, CTRA+ considers the spirals on a plane tilted by an angle $\phi$ with respect to the horizon. By projecting the UAV's velocity vector $v(t)$, we can get its three components:

$$v_x(t) = \frac{dx}{dt} = v(t) \cos(\theta(t)) \cos(\phi(t)) \quad (3)$$
$$v_y(t) = \frac{dy}{dt} = v(t) \sin(\theta(t)) \cos(\phi(t)) \quad (4)$$
$$v_z(t) = \frac{dz}{dt} = v(t) \sin(\phi(t)) \quad (5)$$

Therefore, the velocity’s magnitude $v(t)$ is given by:

$$v(t) = (v_x(t))^2 + (v_y(t))^2 + (v_z(t))^2 \quad (6)$$

In order to compute the position at any time, we need to integrate the velocity components over time:

$$x(t) = x(0) + \int_0^t v(\tau) \cos(\theta(\tau)) \cos(\phi) d\tau \quad (7)$$
$$y(t) = y(0) + \int_0^t v(\tau) \sin(\theta(\tau)) \cos(\phi) d\tau \quad (8)$$
$$z(t) = z(0) + \int_0^t v(\tau) \sin(\phi) d\tau \quad (9)$$

We note that the procedure is equivalent to 2D CTRA \cite{19} for the $x$ and $y$ components, except for the constant multiplying factor $\sin(\phi)$. Hence, the CTRA+ state is given by:

$$x_{CTRA+}(t) = [x(t) \ y(t) \ z(t) \ \theta(t) \ \phi(t) \ \omega(t)]^T$$

which corresponds to the tuple representing the current attitude, with the addition of the velocity $v$, the acceleration $a$, and the turn rate $\omega$.

B. The 3D-CTRA model

The 3D-CTRA model extends the above description by adding a constant tilt rate $\psi = \frac{d\phi}{dt}$. Consequently, the UAV's movement is represented as the combination of two independent spiraling motions on the horizontal and vertical planes, forming a curved helix. While the evolution of $\theta(t)$ still follows \cite{11}, the pitch is given by:

$$\phi(t) = \phi(0) + \psi t \quad (11)$$
Applying the Werner formula, we obtain
\[ y(t) = x(0) + \int_0^t v(t) \cos(\theta(t)) \cos(\phi(t)) dt, \]
which can be solved in closed form. The derivations for \( \omega \) then, when \( \omega \) is a special case equivalent, define the full non-linear version of \( \psi \) when \( \omega \) becomes:
\[ z(t) = z(0) + \sin(\phi(t)) \left( v(t) t - \frac{a \tau^2}{2} \right). \]

Then, when \( \omega = \psi \), i.e., when the rotation on the two axes have the same period, the values of \( x(t) \) and \( y(t) \) become:
\[ x(t) = \left[ \frac{v(\tau) \sin(\theta(t) + \phi(t))}{2(\omega + \psi)} + \frac{a \cos(\theta(t) + \phi(t))}{2(\omega + \psi)^2} + \left( \frac{v(\tau) \tau}{2} - \frac{a \tau^2}{4} \right) \cos(\theta(t) - \phi(t)) \right]^4 + x(0), \]
\[ y(t) = \left[ -\frac{v(\tau) \cos(\theta(t) + \phi(t))}{2(\omega + \psi)} + \frac{a \sin(\theta(t) + \phi(t))}{2(\omega + \psi)^2} + \left( \frac{v(\tau) \tau}{2} - \frac{a \tau^2}{4} \right) \sin(\theta(t) - \phi(t)) \right]^4 + y(0), \]

The case in which \( \omega = -\psi \) produces a similar result, with inverted terms. Setting \( t = T \), \[ (11), (12), \] and \[ (13)-(16), \] on top of next page, where we used the compact notation \[ F(x) = F(b) - F(a) \] to indicate that the primitive function \( F(x) \) should be evaluated at the extremes \( a \) and \( b \).

Finally, three special cases need to be considered. First, when \( \psi = 0 \), i.e., when the model is equivalent to \( \text{CTRA} \) and the pitch is constant, the value of \( z(t) \) becomes:
\[ z(t) = z(0) + \sin(\phi(t)) \left( v(t) t - \frac{a \tau^2}{2} \right). \]

This complicates the derivation of the motion equations considerably, since \( \phi(t) \) is now time-dependent. For the sake of simplicity, we report the procedure only for \( x(t) \), which is given by
\[ x(t) = x(0) + \int_0^t v(\tau) \cos(\theta(\tau)) \cos(\phi(\tau)) d\tau. \]

C. Remote tracking and communications

As in [19], the tracking process is implemented by the UnScented Kalman Filter (UKF) algorithm. In particular, we assume that the UAV and the control station are equipped with two UKF [23]. While the drone exploits the measurements provided by its on-board sensors to track its own state, the control station’s UKF has no input but the information received from the UAV. We adopt a periodic broadcasting strategy [18]: the UAV sends the estimate of its own state to the control station with a constant inter-transmission period. After it receives an update, the control station updates its UKF with the new information and exploits the predictive step to forecast the UAV’s trajectory. Naturally, the errors will compound, causing long-term predictions to become less and less accurate until the next update.

In order to enable the UAV to send the UKF parameters even at great distances, we considered the LoRaWAN technology [26], which leverages the proprietary LoRa PHY modulation which is based on a chirp spread spectrum technique to transmit over long distances. The performance of the modulation can be tuned through the SF parameter, which takes values from 7 to 12, and allows to trade coverage range for data rate: signals transmitted with higher SFs values require longer transmission times, but are more robust to channel impairments and, thus, can be received at farther distances, up to several kilometers in open-air scenarios.

LoRaWAN is based on a star topology, with three kinds of devices:

- the Network Server (NS) which is the central network controller;
- the End Devices (EDs), peripheral nodes, collecting data and transmitting them through the LoRa modulation;
- the Gateways (GWs) acting as relays between EDs and NS, collecting messages from devices and forwarding them to the controller through a legacy IP connection, and vice-versa.

We assume that the drone is equipped with a LoRaWAN Class A ED. This class is designed to consume a minimum amount of energy, staying in sleep mode most of the time, transmitting when necessary, and opening two short windows for reception after each transmission. LoRaWAN works in the unlicensed 868 MHz sub-band, which is subject to Duty Cycle (DC) regulations. In particular, three 125 MHz channels are allocated to Uplink (UL) transmissions, and must respect a DC limitation of 1%. Another option is to use a single 250 MHz channel, which does not bring the benefits of frequency orthogonality but reduces the packet transmission time, and is preferable in case of a system with a single drone.

Because of the DC limitation, we need to compress the system state to reduce the inter-transmission time and improve the tracking performance. In order to minimize the payload size, we can represent the position using 2 bytes, allowing movement in a square box with a size of 13 km while limiting the quantization error to 10 cm, significantly less than the average GPS error. Angles and turn rates can be represented using just 1 byte, with a maximum error of 0.7 degrees;
is described by the matrix $Q = qI$, where $I$ represents the identity matrix. Instead, the error affecting the drone measurements is given by a diagonal matrix $R$, whose elements represent the accuracy of the various drone sensors. The noise matrices and the UKF parameters are reported in Tab. II. In particular, values of $R$ were chosen according to [28]–[30]. We highlight that the UKF setting, e.g., the state dimension, changes according to the chosen motion model. As already stated, the UKF at the control station is used to estimate the target trajectory by exploiting only the predictive step. This implies that, when a new update is received, the filter state is substituted with the new information, and the estimation process starts again.

The scenario of interest was studied with the network simulator ns-3, with a single drone moving in the space according to the mobility traces of [31]. The drone was equipped with a LoRaWAN interface, which transmitted packets at the standard frequency plan. These messages were collected by a GW and forwarded to a NS. Transmitted packets did not require any acknowledgment, and the NS did not control any of the communication parameters. For each packet, we recorded whether it was successfully received or not, and estimate the tracking performance. We also moved the initial position of the GW to see how much the tracking performance was affected by the communication limitations. In the rest of the section, we will analyze the positioning error for different tracking and communication scenarios. In particular, we investigate our tracking scheme for different values of the SF and of the initial distance $d$ between the UAV and the GW.

### B. Results

First, we consider the 30 s drone trajectory shown in Fig. 2. The same figure includes the trajectories estimated by the control station using the DR and 3D-CTRA motion models, considering a communication setup with $d = 1000$ m, SF = 7 and $B = 250$ MHz. Comparing the different trajectories,
we observe how the [DR] scheme does not follow the target while the [3D-CTRA] scheme has smaller deviations from the real trajectories. This is confirmed by the results in Fig. 3 which shows the base station tracking error over time for all the considered models. We highlight that the error of the [DR] model rapidly increases every time the drone performs non-linear movements, as it happens at time $t \approx 6, 12, 19$ s. Instead, the error of both the [CTRA+] and the [3D-CTRA] models presents a smoother trend, with fewer and lower peaks.

From here on, we consider the cumulative results over all the available trajectories. Fig. 4 shows the boxplot of the position error along the three axes with SF = 7, $d = 1000$ m, and $B = 250$ MHz. We observe that, when considering the $X$ and $Y$ axes, the [3D-CTRA] model always outperforms both the [DR] and the [CTRA+] models, thanks to its richer representation of the drone’s movements. As expected, [CTRA+] also outperforms [DR] since it uses the same model as [3D-CTRA] on the horizontal plane. Surprisingly, when considering the $Z$ axis, the [DR] system shows a slightly lower error than [CTRA+] and [3D-CTRA]. This might be due to climbs and dives being relatively rare, so [DR]’s more frequent updates could give it a slight edge over [3D-CTRA]. On this axis, [CTRA+] performs worst, because it combines the lower update frequency of [3D-CTRA] and the inaccurate model of [DR].

We now evaluate how the communication parameters can affect the performance of the tracking system. Fig. 5 shows the boxplot of the positioning error for different values of $d$ and considering SF = 7 and $B = 250$ MHz. It is easy to see that [3D-CTRA] outperforms the other approaches, even if its updates are less frequent. In particular, considering $d = 1000$ m, the 75th percentile of the error obtained with the [3D-CTRA] model is 30% lower than [DR]’s and 10% lower than [CTRA+]’s. We observe that all the systems guarantee an average error below 2 m for both $d = 1000$ m and $d = 2000$ m. However, the error dramatically increases when considering $d = 3000$ m for all the considered schemes, since the drone is too far away from the control station for SF = 7 and several packets are lost. However, [3D-CTRA] is still the best option: it is the only one to guarantee an average error below 5 m.

To allow the control station to accurately predict the drone’s trajectory at larger distances, it is necessary to adopt a more robust communication setting. In Fig. 6 we report the results we obtained for $d \in \{1000, 2000, 3000\}$, with SF = 8 and $B = 250$ MHz. Since we increased the SF, the bitrate is lower, and the drone transmits its state less frequently. As expected, this implies that the positioning error increases at short distances.
For \( d = 1000 \text{ m} \) and \( d = 2000 \text{ m} \), the 3D-CTRA model guarantees lower error than the DR model but presents similar results to the CTRA+ model. Instead, in the case of \( d = 3000 \text{ m} \), 3D-CTRA outperforms both the other techniques: the 75th percentile error obtained with the 3D-CTRA is 20% lower than DR's and 12.5% lower than CTRA's.

Finally, comparing Fig. 3 and Fig. 6 shows how a more robust scheme greatly improves the tracking performance when the distance between the control station and the UAV is large. It is worth noting that LoRaWAN also provides a Data Rate Adaptation mechanism, where the SF employed by the device is set by the controller: in this way, it is possible to benefit from the increased coverage range achieved with higher SF when necessary, and go back to lower SFs when the UAV is closer to the GW to increase the frequency of transmission messages. Therefore, adapting the SF dynamically will be the best choice in a real scenario, providing significant performance gains. However, the reactiveness of the adaptive mechanism should be carefully tuned to avoid instability.

V. CONCLUSIONS AND FUTURE WORK

In this work, we presented a tracking system for UAVs based on a novel 3D-CTRA mobility model and on periodic transmissions over LoRaWAN. Our system can track a drone's trajectory with high accuracy even when the drone is at 3 km from the LoRaWAN gateway, and the mobility models we propose significantly outperform standard DR. Moreover, LoRaWAN’s duty cycle limit is suited to manage swarms of dozens of drones, as it prevents traffic congestion.

There are several possible avenues of future work: a refinement of the movement model, including maneuver and mission-level information, might reduce the tracking error. From the communication side, it would be interesting to investigate the tracking performance with different data rate adaptation algorithms, as well as explore features that are not part of the LoRaWAN standard up to now, like the use of a different frequency plan or of listen-before-talk instead of applying the duty cycle. Finally, the study of the behavior of swarms, and possible strategies to avoid packet collision, is another interesting option that would enable new applications by improving the tracking accuracy at low cost.

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