Charge Order Breaks Magnetic Symmetry in Molecular Quantum Spin Chains

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Charge order affects most of the electronic properties but is believed not to alter the spin arrangement since the magnetic susceptibility remains unchanged. We present electron-spin-resonance experiments on quasi-one-dimensional (TMTTF)$_2$X salts (X = PF$_6$, AsF$_6$ and SbF$_6$), which reveal that the magnetic properties are modified below $T_{CO}$ when electronic ferroelectricity sets in. The coupling of anions and organic molecules rotates the g-tensor out of the molecular plane creating magnetically non-equivalent sites on neighboring chains at domain walls. Due to anisotropic Zeeman interaction a novel magnetic interaction mechanism in the charge-ordered state is observed as a doubling of the rotational periodicity of $\Delta H$.

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INTRODUCTION

Charge disproportionation is a common ordering mechanism in correlated electron systems that is intensively investigated in transition-metal oxides as well as organic compounds [1, 2] because it is recognized to influence charge, lattice and magnetic degrees of freedom. For static charge order (CO) the electrons are (partially) localized resulting in an insulating state, most evident in manganites or at the 1/8 anomaly observed in cuprates [3]. Fluctuating stripes, however, may be relevant for high-temperature superconductivity [4], but also in organic systems evidence accumulates that charge fluctuations mediate superconductivity [5].

As far as the magnetic properties are concerned, the situation is even more puzzling. CO can induce ferroelectricity when the inversion symmetry is broken, as suggested (and also disputed) for some mixed-valence oxides [6,7], magnetite [8–10], manganites [11,12] or nickelates [13,14]. For perovskites, however, there seems to be a mutual exclusion of magnetism and ferroelectricity [15,16], albeit the field of multiferroics drew enormous attention over the last years [17,18]. About ten years ago, electronic ferroelectricity was discovered in quasi-one-dimensional organic compounds (TMTTF)$_2$X (where TMTTF stands for tetramethyltetrathiafulvalene and X denotes a monovalent anion such as PF$_6$, Br) around 50 – 160 K [12]. X-ray investigations could not identify any superstructure, on this account it is known as a “structureless” transition [20].

In these strongly correlated electron systems, nearest-neighbor Coulomb repulsion causes CO upon cooling below $T_{CO}$ characterized by a charge gap in the transport properties [21]. From the magnetic point of view, these are $S = 1/2$ antiferromagnetic chains with some ordering at low temperatures [22,23]. Surprisingly, by now no indications of the CO transition could be observed in the magnetic properties, such as spin susceptibility (cf. Fig. [1]). Here we report comprehensive electron spin resonance (ESR) investigations that reveal a novel magnetic interaction mechanism caused by charge disproportionation; we observe first evidence that charge order breaks the symmetry of the magnetic degree of freedom in these quantum spin chains.

RESULTS AND ANALYSIS

Single crystals of (TMTTF)$_2$X with octahedral anions $X = \text{PF}_6$, $\text{AsF}_6$, and $\text{SbF}_6$, are grown electrochemically. The planar TMTTF molecules stack in a slight zig-zag fashion normal to the molecular plane; this $a$ axis is the best-conducting direction. The stacks are arranged next to each other with some minor interaction in $b$ direction and separated in the $c$ direction by the anions. Since one electron is transferred to each anion, the organic molecules are left with half a hole, on average. Triggered by the $A_2B$ stoichiometry, the TMTTF molecules form dimers along the $a$-axis; a fact that enhances the charge localization observed as a broad minimum in resistivity at $T_p \approx 250$ K [22,28]. In Fig. (a)-(c), $\rho(T)$ is plotted for the three compounds under consideration [21].

In addition, basically all TMTTF salts develop charge imbalance for $T < T_{CO}$, resulting in charge-rich $(0.5e + \delta)$ and charge-poor molecules $(0.5e - \delta)$ as first proven by nuclear magnetic resonance [29]. The charge disproportionation can be best visualized by the splitting of the intramolecular vibration $\nu_{28}(B_{1u})$ plotted in Fig. (d)-(f) [31]. The results are summarized in Tab. for further details, see Ref. [24].

Charge order causes an additional gap to open in the density of states at $T_{CO}$, leading to a kink in the electrical resistivity $\rho(T)$ indicated by arrows in Fig. (a)-(c); as the temperature decreases it evolves in a mean-field fashion to $\Delta_{CO}(T \rightarrow 0) \approx 745$ K, for the example of (TMTTF)$_2$SbF$_6$ [21].

Although the effect of charge ordering on the spin degree of freedom has attracted considerable attention from the theoretical side [32], it is not completely clear how the spin and orbital magnetic moments behave in the
J responds to fits using the model \([29]\) of a Heisenberg chain with a ground state. In contrast, \((TMTTF)\) localization at temperature-dependent dc resistivity \(\rho\) the three compounds \((TMTTF)\) spin susceptibility \((TMTTF)\) \(T\) the magnetic field and by rotating around the molecular axis \((\text{cf. Fig. 6})\). In Fig. 2 the linewidth \(\Delta\) the temperature range from 4 to 300 K at different orientations of the anisotropy arises from spin-orbit coupling of the conduction electrons \([33,34]\); in other words the arrangement of the \(g\)-tensor can be solely deduced from the molecular symmetry. At room temperature the \(g\)-factor and linewidth are maximum when the external magnetic field is oriented along the molecular axis \(\tilde{c}\), while \(g\) and \(\Delta H\) are smallest when measured normal to the \((\text{Fig. 2})\).

The obtained coupling constants \(J\) are listed in Tab. I.

We have performed comprehensive multifrequency ESR investigations (X-, Q- and W-band) in the temperature range from 4 to 300 K at different orientations of the magnetic field and by rotating around the molecular axes (cf. Fig. 6). In Fig. 2 the linewidth \(\Delta H(T)\) and the \(g\)-shift (from the free electron value \(g_e = 2.002319\)) are plotted as a function of temperature for the example of \((TMTTF)\) \(\Delta H(T)\) becomes weaker.
indicates an additional interaction channel to develop for $T < T_{CO}$. Basically the same behavior at $T_{CO}$ is observed for (TMTTF)$_2$AsF$_6$, while for (TMTTF)$_2$PF$_6$ the effect is smaller due to stronger coupling $J$ and lesser charge imbalance $2\rho$, which coincide with the much lower transition temperature $T_{CO}$ and almost vanishing charge gap $\Delta CO$, summarized in Tab. 1.

In order to gain more insight how charge order affects the spins, we performed detailed angular-dependent measurements of $\Delta H$ and $\Delta g$ at selected temperatures. While the rotational symmetry of the $\Delta g$ remains unchanged with temperature, $\Delta H$ exhibits a very unusual behavior as demonstrated in Fig. 3. For $T > T_{CO}$ the $g$-factor and the linewidth are dominated by spin-phonon scattering with an angular dependence [22]

$$\Delta H_{sp}(\theta) = \left[ \Delta H_{sp}^2(\hat{a}) \cos^2 \theta + \Delta H_{sp}^2(\hat{b}) \sin^2 \theta \right]^{1/2}$$

(1)

in the $\hat{a} \hat{b}$ plane, for instance. Most remarkably, the periodicity doubles as the charge-ordered state is entered. In the CO state the orientational dependence of the linewidth can be fitted by the sum of Eqs. 1 and 2:

$$\Delta H_{mod}(\theta) = \Delta H_{mod}(45^\circ) \sin \{2\theta\}$$

(2)

where $\Delta H_{mod}$ is the excess linewidth. The enhancement of the linewidth observed in the diagonal direction $\Delta H_{en} = \Delta H(45^\circ) - \frac{1}{2} \Delta H(\hat{a}) + \Delta H(\hat{b})$ becomes more pronounced as the frequency $\nu$ increases, as depicted in Fig. 4. The quadratic behavior

$$\Delta H_{en}(\nu) = A + B\nu^2$$

(3)

strongly indicates anisotropic Zeeman interaction [36]. The same period doubling in $\Delta H(\theta)$ can be observed in our X-band experiments on (TMTTF)$_2$PF$_6$, although the effect is much weaker.

In the case of staggered fields, antisymmetric Dzyaloshinskii-Moriya interaction also causes a $\nu^2$ frequency dependence of the linewidth; however, leading to a $T^{-2}$ temperature dependence [37, 38] in contrast to our findings. Note also that in those references Heisenberg spin chains with significant intra-chain Dzyaloshinskii-Moriya interaction were considered. In the present case, the alternating contributions result from interaction between the chains, for which the isotropic exchange $J$ is already small. Thus the antisymmetric Dzyaloshinskii-Moriya exchange can be neglected.

From similar observations on inorganic linear-chain compounds, Pilawa derived a contribution of the anisotropic Zeeman interaction to the linewidth [39]

$$\Delta H_{AZ} = -\frac{\mu_B H_0^2}{g \cdot k_B J'} \sqrt{ \frac{\pi}{8} |\Delta g|^2 }$$

(4)

where $J'$ is the exchange interaction between two inequivalent magnetic sites on the neighboring chains; $\Delta g$ is the difference between their $g$-tensors. In our case the interchain exchange constant is $J' = 1.1$ K [40]. With $B_0 = 33.6$ kOe for the W-band, we obtain $\Delta g = 7.82 \times 10^{-3}$ and $16.78 \times 10^{-3}$ for (TMTTF)$_2$AsF$_6$ and (TMTTF)$_2$SbF$_6$, respectively [41]. The fact that we do not observe two distinct but only a single Lorentzian line implies that the hopping rate between the non-equivalent sites is much larger than the splitting (strong-coupling limit). The difference in Larmor frequencies in the W-band $\Delta \nu = (\Delta g/g) \times 95$ GHz corresponds to only 27 mK, which is much smaller than $J'$.

The magnetically inequivalent sites have to be located on adjacent stacks; intrachain interaction is so strong.
that it would suppress the anisotropic Zeeman effect at these frequencies. From the fact that the maximum of $\Delta H$ occurs at $\theta = 45^\circ$ and that $\Delta g$ is not zero, we conclude that the g-tensors of the two sites do not coincide with the principle magnetic axes any more but are rotated around the $\hat{c}$ axis by an angle $\phi$ in opposite directions as depicted in Fig. 5 at temperature well below $T_{\text{CO}}$ we obtain $\phi = \pm 22^\circ$ for $X = \text{PF}_6$, AsF$_6$ and $\pm 32^\circ$ for (TMTTF)$_2\text{SbF}_6$, respectively [42].

**DISCUSSION**

The crucial question now is, why CO triggers a rotation of the g-tensors. ESR experiments by Furukawa et al. [34] revealed that the Coulomb potential of the anions influences the electronic wavefunctions on the TMTTF molecules. Depending on whether the adjacent molecules are charge rich or charge poor, this constitutes non-equivalent charge and spin distributions as sketched in Fig. 5. The imbalance of the spin density causes a rotation of the g tensor by an angle of $\phi$. Our findings are in accord with the suggestion by Riera and Poilblanc [43] that charge order in TMTTF salts is a cooperative effect between the Coulomb interaction and the electronic coupling of the TMTTF stacks to the anions [44].

The occurrence of spontaneous dipole moments [19] and second harmonic generation [45] evidences the loss of inversion symmetry (with one center located at the anions, for instance) for $T < T_{\text{CO}}$. Our vibrational spectra (Fig. 1) show the presence of charge-rich and charge poor molecules, which, however, can be arranged on the dimerized stacks in two possible ways: $++$ or $--$. This immediately implies that the rotation of the g tensor can occur in both directions $\pm \phi$. Thus at $T < T_{\text{CO}}$ domains are formed with inequivalent magnetic sites on neighboring stacks at the boundaries, as depicted in Fig. 5. Without interaction two distinct ESR signals are expected below $T_{\text{CO}}$, but the strong coupling leads to a significant broadening, that might get resolved by going to even higher frequencies.

Structural investigations could not identify any superstructure or change in symmetry, however, a strong increase in mosaicity at $T_{\text{CO}}$, as shown in Fig. 7 [51]. We conclude that the ordering occurs on a local scale with nanometer-sized CO domains. Similar, but larger ferroelectric domains of electronic origin have been directly observed in the two-dimensional organic compound $\alpha$-(BEDT-TTF)$_2\text{I}_3$ below the CO transition [16].

As the averaged g-tensor does not abruptly change at $T_{\text{CO}}$, the charge ordering can be pictured as follows: For $T > T_{\text{CO}}$ random charge disproportionation exists on the TMTTF stacks giving rise to an averaged g-factor as observed, but without any anisotropic Zeeman effect, which is suppressed due to narrowing by large intrachain exchange. Below $T_{\text{CO}}$, the charge imbalance becomes cooperative within each stack; there is some weak interaction of adjacent chains. At the boundary of the stacks defined by the direction of charge and spin distortion, translational symmetry is lost. This gives rise to two inequivalent chains that yield the same averaged g-tensor along the $\hat{a}$ and $\hat{b}$ axes as above $T_{\text{CO}}$. In the diagonal directions, however, the anisotropic Zeeman effect now becomes visible in our ESR data because the signal is narrowed by the much weaker interchain exchange.

**CONCLUSIONS**

In summary, the charge order observed in the linear-chain compounds (TMTTF)$_2X$ by the splitting of the molecular vibrations opens a gap in the charge excitations. It also affects the magnetic behavior via mutual interaction with the anions. For $T < T_{\text{CO}}$ the inversion symmetry is broken; charge disproportionation leads to a different electronic distortion on the organic molecules that eventually rotates the g-tensors, with two directions $\pm \phi$ possible. From our multifrequency ESR measurements we conclude that in the charge-ordered regime two inequivalent magnetic TMTTF chains coexist, which produce a doubling in the angular periodicity of the linewidth as well as the characteristic quadratic frequency dependence. Thus, our experiments show that
charge order not only causes ferroelectricity but can also break the symmetry of the magnetic degree of freedom in quantum spin chains.

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Appendix A: Structure

The Fabre salts (TMTTF)$_2$X are charge-transfer salts consisting of stacks of the planar organic molecules TMTTF (which stands for tetramethyltetra-thiafulvalene) along the $a$-axis that are separated in $c$ direction by monovalent anions $X$. The overlap of the $\pi$ orbitals in $a$ direction makes them model systems of one-dimensional metals. In $b$-direction the distance of the stacks is comparable to the van der Waals radii. Basically no coupling between the molecular stacks exists in the $c$ direction. In the case of the Bechgaard salts the TMTSF molecule contains selenium instead of sulphur with more extended orbitals, leading to better metallic conduction and even superconductivity [26, 47–49].

All compounds of the TMTTF family are isostructural (triclinic P1 space group, $C_1$ symmetry with $Z = 1$) with the TMTTF stacked normal to the molecular plane in $a$ direction, slightly displaced in $c$ direction to optimize the orbital overlap of the selenium atoms along $a$. In spite of the $A_2B$ stoichiometry and the corresponding dimerization, the separation of the TMTTF molecules along the stacks only differs by approximately 3% at room temperature and even less at low temperature [21, 50], implying almost equal overlap integrals along the $a$ axis. Due to the triclinic symmetry, $b'$ commonly denotes the projection of the $b$ axis perpendicular to $a$, and $c'$ is normal to the $ab$ plane. Here we introduce a Cartesian coordinate system linked to the TMTTF molecule, with $\hat{a}$ points normal to the molecular plane, $\hat{c}$ is the extended molecular axis, and $\hat{b}$ is perpendicular to both (cf. inset of Fig. 2). In a good approximation $\hat{a}$ is parallel to the stacking axis $a$, and $\hat{c}$ is almost $c+b$, as depicted in Fig. 6.

X-ray investigations of (TMTTF)$_2$SbF$_6$ single crystals performed at different temperatures down to $T = 80$ K rule out a structural transition at the charge-order temperature [51], confirming previous attempts by C. Coulon and collaborator [21, 51, 52]. Structural data do not unambiguously reveal the loss of inversion symmetry. Their analysis, however, yields a marginal better fit with no symmetry restrictions; but this also holds (to a minor degree) at room temperature. Charge order does not constitute a superstructure; nevertheless, the spots broaden significantly upon cooling with a distinct change at $T_{CO}$. This is a measure of the mosaicity of the sample: in Fig. 7 the temperature dependence of the mosaicity is plotted normalized to the room-temperature value. We interpret this as the development of domains with the SbF$_6$ anions slightly distorted in one or the other direction. The distortion, but also the domain size changes with temperature leading to a maximum around $T_{CO}$. Typical for an effect of disorder, the phenomenon depends on cooling rate and slightly vary from crystal to crystal.

Appendix B: Experimental Details

Single crystals of (TMTTF)$_2$X with $X = PF_6$, AsF$_6$, and SbF$_6$ were grown by electrochemical methods in an H-type glass cell at room temperature [53]. A constant voltage of 1.5 V was applied between platinum electrodes with an area of approximately 1 cm$^2$. The current through the solution was between 1 and 2 $\mu$A. After several weeks we were able to harvest needle-shaped single crystals of several millimeters in length and less than a millimeter in width.

The electrical transport was characterized by dc resistivity measured as a function of temperature in all three directions [21]. We evaporated small gold contacts onto the natural crystal surface and attached thin gold wires by carbon paste. Along the long $a$ axis of the crystals and also for the $b$ direction four-point measurements could be performed, while for the $c$ direction two contacts were applied on opposite sides of the crystal. The samples were attached to a sapphire plate in order to ensure good thermal contact and slowly cooled down to helium temperatures.

Measurements of the magnetic susceptibility were performed using a Quantum Design SQUID (superconducting quantum interference device) magnetometer between 1.8 and 380 K. A large number of single crystals were glued parallel to each others inside a plastic straw using vacuum grease, the magnetic field was applied parallel to the $a$ axis. The background signal of the sample holder and the vacuum grease was measured separately and subtracted in order to obtain the intrinsic magnetization of the sample. To estimate the spin susceptibility, we subtracted a temperature independent diamagnetic contribution of the core electrons $\chi_{dia} = -5.3 \times 10^{-9}$ m$^3$/mole from the original data of all specimen under consideration.

The infrared reflectivity spectra polarized along the $c$ direction were recorded by utilizing a Bruker IFS 66v/s and a Bruker Vertex 80 Fourier transform spectrometer extended with a IR microscope HYPERION which is purged with nitrogen to suppress any disturbing influence.
The electron spin resonance (ESR) spectra were carried out in a continuous wave X-band spectrometer Bruker ESP 300 at 9.5 GHz and a W-band spectrometer Bruker Elexys 680 at 95 GHz at Stuttgart University, and a Q-band spectrometer Bruker Elexys 500 at 34 GHz at Augsburg University. Complementary X-band measurements were performed at the Hochfeld-Magnetlabor Dresden. The temperature dependence of the ESR properties was measured down to $T = 4$ K by utilizing continuous-flow helium cryostats. The typical size of the single crystals used in the X-band ESR measurements was $2 \times 0.5 \times 0.1$ mm$^3$, while very small samples of less than $0.4 \times 0.4 \times 0.05$ mm$^3$ were used in the Q- and W-band ESR measurements in order to avoid any sample-size effect that can lead to a broadening of the linewidth.

### Appendix C: Magnetic Characterization

The large thermal expansion of the organic compounds has strong effects on the temperature dependence of the spin susceptibility. To compare the experimental results (usually obtained at $p = \text{const}$) with the theoretical predictions (in general calculated for $V = \text{const}$), the spin susceptibility at constant pressure $(\chi_s)_p$ has to be transformed in the spin susceptibility at constant volume $(\chi_s)_V$. In the case of (TMTSF)$_2$PF$_6$ the temperature dependence of $(\chi_s)_V$ was estimated by Wzietek et al. from NMR and x-ray measurements under pressure. We assumed that the substitution of sulfur for selenium and the exchange of the inorganic anions has no considerable influence on the thermal expansion, thus we took the ratio $(\chi_s)_V/(\chi_s)_p$ for different temperatures to rescale our susceptibility data of (TMTTF)$_2$X.

![Crystal structure of (TMTTF)$_2$SbF$_6$, as an example, viewed (a) along the stacking direction $a$, (b) along the $b$ axis and (c) along the $c$ direction. The strongest coupling between the octahedral anions and the sulfur atoms are indicated by the red dashed lines I and II which are related by inversion symmetry for $T > T_{CO}$. In the charge-ordered state, not only the TMTTF molecules develop a charge disproportionation with alternating charge-rich and charge-poor molecules along the stacks, also the octahedral anions are slightly distorted. The inversion symmetry is lifted and contact I becomes stronger than II, for instance. Two kind of domains are formed separated by domain walls preferentially in the $ab$ or $ac$ planes. Also shown is the configuration between the TMTTF molecular structure and the principal axes of the $g$-tensor. Note there exists only one electron per dimer. At elevated temperatures the $g$-tensor (blue arrows indicate the principal magnetic directions $\hat{a}$, $\hat{b}$ and $\hat{c}$) is determined by the molecular structure. The $\hat{a}$ axis of the $g$-tensor is normal to the molecular plane and along the stacking direction, while the $\hat{c}$ axis points along to the longest molecule extension. For $T < T_{CO}$ the principal axes of the $g$-tensor rotate around the $\hat{c}$-axis by an angle $\phi$ in opposite directions, resulting in the brown arrows.](image)

![Temperature dependence of the normalized mosaicity of (TMTTF)$_2$SbF$_6$ and (TMTTF)$_2$PF$_6$ determined from the width of the x-ray spots (after Ref. 51). When the temperature drops below 200 K, the mosaicity of (TMTTF)$_2$SbF$_6$ increases dramatically approaching a maximum at the charge order temperature $T_{CO} = 157$ K. For comparison the behavior of (TMTTF)$_2$PF$_6$ is also presented where only a small increase is observed. Note, in the case of (TMTTF)$_2$PF$_6$ the phase transition happens only at $T_{CO} = 67$ K.](image)
At high temperatures the spin susceptibility at constant volume of (TMTTF)$_2$X resembles the well-known behavior of a spin-1/2 Heisenberg chain with antiferromagnetic coupling as depicted in Fig. 1 by the dashed blue lines. The thermodynamic and magnetic properties of such a system were studied by Bonner and Fisher [57]. The advanced model of Eggert, Affleck, and Takahashi [29] using the Bethe ansatz differs appreciably only at low temperatures ($T < 0.2J$). For $T > 100$ K the ESR intensity at constant volume can be modeled using $J = 420$, 410, and 400 K for (TMTTF)$_2$PF$_6$, (TMTTF)$_2$AsF$_6$ and (TMTTF)$_2$SbF$_6$, respectively.

The temperature dependence of the ESR results along the three crystal axes of (TMTTF)$_2$PF$_6$, (TMTTF)$_2$AsF$_6$ and (TMTTF)$_2$SbF$_6$ are shown in Fig. 9. The g-shift $\Delta g(T) = g(T) - 2.002319$ for all three crystal axes is very small. At elevated temperatures, the g values show no significant temperature dependence but a distinct anisotropy with a negative value of $\Delta g$ along the chain direction $\hat{a}$ and positive values perpendicular to the chain direction, as seen in Fig. 8. This behavior is found in all TMTTF and TMTSF salts as presented in Refs. [22][23]. In all cases the small anisotropy of $\Delta g$ between the $\hat{b}$ and $\hat{c}$ axes increases with temperature. The g value is largest for $B_0 \parallel \hat{c}$ and closest to the free-electron value parallel to the stacks. As the temperature is lowered, the linewidth $\Delta H$ decreases almost linearly with $T$ in all directions. In the $\hat{c}$ direction $\Delta H(T)$ is slightly larger; the most narrow lines are always observed along the chains.

At low temperatures (TMTTF)$_2$PF$_6$ and (TMTTF)$_2$AsF$_6$ undergo spin-Peierls transitions at $T_{SP} = 19$ and 13 K, respectively. The formation of states with singlet-paired holes due to the tetramerization causes a decreasing susceptibility with an exponential drop of the intensity down to lowest temperatures, but it does not completely vanish (Fig. 1). This phase transition also leads to a broadening of the ESR linewidth and a small change in the g values [22]. (TMTTF)$_2$SbF$_6$, on the other hand, orders antiferromagnetically at $T_N = 8$ K, leading to a decrease in $\chi_s(T)$ with decreasing temperature before it eventually turns up again. This phase transition is accompanied by a decrease in the g-shift for the $\hat{b}$ and $\hat{c}$ axes; along the $\hat{a}$ axis the g factor becomes larger below $T \approx 15$ K. The low-temperature ordered states are out of the scope of the present paper and discussed elsewhere [22][54].

FIG. 8: Angular dependence of the g-value of (TMTTF)$_2$SbF$_6$ at room temperature measured at X-band frequency when the static magnetic field $B_0$ is rotated within the $\hat{ab}$ plane (green circles), the $\hat{bc}$ plane (red squares), and the $\hat{ac}$ plane (blue triangles). The least-square fits by $g(\theta) = (g^2_{\min} \cos^2 \theta + g^2_{\max} \sin^2 \theta)^{1/2}$ are shown by the corresponding lines.

From the fact that the maximum of $\Delta H$ occurs at the diagonal direction $\theta = 45^\circ$ of the $\hat{ab}$ plane and that the g-values of neighboring molecules differ by $\Delta g$ we conclude that the g-tensors of the spins corresponding to the two different magnetic sites do not coincide with the principle magnetic axes. They are rotated around the $\hat{c}$ axis by $\phi$ in opposite directions as depicted in Fig. 8. As shown in Fig. 9 the two different sites contribute to the observed g-value according to

$$g_1 = \left( g^2_{\max} \cos^2 \theta - \phi + g^2_{\min} \sin^2 \theta \right)^{1/2} \quad (5)$$

$$g_2 = \left( g^2_{\max} \cos^2 \theta + \phi + g^2_{\min} \sin^2 \theta \right)^{1/2} \quad (6)$$

where $g_1$ and $g_2$ correspond to the g-tensor of type 1 and type 2 spins, respectively. The principal axes of the two kinds of spins span the angle $\phi$. $g_{\max}$ and $g_{\min}$ are the maximum and the minimum of the g-values for each kind of spins at the angle $\phi$, respectively. For symmetry reasons the g values have to be identical $g_1 = g_2$ at $\theta = 0^\circ$ and $\theta = 90^\circ$, while at $\theta = 45^\circ$ the difference of the g values is obtained from the anisotropic Zeeman effect. We obtain for (TMTTF)$_2$PF$_6$ $g_{\max} = 2.0117$, $g_{\min} = 2.0008$, and $\phi = 22^\circ$; for (TMTTF)$_2$AsF$_6$ $g_{\max} = 2.0071$, $g_{\min} = 1.9999$, and $\phi = 22^\circ$; and for (TMTTF)$_2$SbF$_6$, where $\phi = 32^\circ$, for the example of (TMTTF)$_2$SbF$_6$.

In Fig. 10 the linewidth of (TMTTF)$_2$PF$_6$. (TMTTF)$_2$AsF$_6$ and (TMTTF)$_2$SbF$_6$ is plotted as a function of angle when the magnetic field is rotated around the $\hat{c}$ axis. While at room temperature (upper frames) the angular dependence follows Eq. (1), $\Delta H$ strongly increases in the diagonal direction ($\phi = \pm 45^\circ$) as $T < T_{CO}$ (lower frames). The effect becomes stronger when going from (TMTTF)$_2$PF$_6$ to (TMTTF)$_2$AsF$_6$ and to (TMTTF)$_2$SbF$_6$, corresponding to the increase in charge disproportionation and transition temperature $T_{CO}$.

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FIG. 9: (Color online) Temperature dependence of (a) the ESR linewidth $\Delta H$, and (b) the $g$-shift $\Delta g(T) = g(T) - 2.002319$ for (TMTTF)$_2$PF$_6$ (left panel), (TMTTF)$_2$AsF$_6$ (middle panel) and (TMTTF)$_2$SbF$_6$ (right panel) measured by X-band spectroscopy along the three directions $\tilde{a}$ (green dots), $\tilde{b}$ (open red squares), and $\tilde{c}$ (blue triangles).

FIG. 10: (Color online) Angular dependence of the X-band ESR linewidth within the $\tilde{a}\tilde{b}$ plane of (TMTTF)$_2$PF$_6$ (left panel), (TMTTF)$_2$AsF$_6$ (middle panel) and (TMTTF)$_2$SbF$_6$ (right panel) measured at (a) room temperature and (b) low temperature, as indicated. The solid lines are obtained from fits of the data by Eqs. (1) and (2). Note the different vertical scale, indicating the observed effect is about ten times as big in (TMTTF)$_2$SbF$_6$ compared to (TMTTF)$_2$PF$_6$.

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