Measurement of the branching fraction of $B^+ \to \tau^+ \nu_\tau$ decays with the semileptonic tagging method and the full Belle data sample

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where $G$ is expected to be the highest purely leptonic branching fraction of $\tau^+ \nu$ because of the helicity suppression and weakly by the factor $f_B$ The purely leptonic decay $B^+ \to \tau^+ \nu_{\tau}$ is the only decay of this kind which has been measured with a significance of more than three standard deviations. All of the inputs of Eq. 1 are measured or, in the case of $f_B$, can be obtained using the methods of lattice quantum chromodynamics. An independent estimation of the branching fraction, which uses $V_{ub} = (3.70 \pm 0.12 \pm 0.26) \times 10^{-3}$, $f_{B^+}/f_{B_s} = (225.6 \pm 1.1 \pm 5.4)$ MeV, and $f_B/f_{B_s} = 1.205 \pm 0.004 \pm 0.007$ as input, gives $B(B^+ \to \tau^+ \nu_{\tau}) = (0.753_{-0.052}^{+0.052}) \times 10^{-4}$ 2.

Physics beyond the SM, such as the presence of additional charged Higgs bosons, could constructively or destructively interfere with the SM weak decay process. Measurements by the BaBar 3, 4 and Belle 5 collaborations showed a slight disagreement with the SM expectation, but the most recent measurement by the
Belle collaboration [6], using a hadronic tagging method, was in very good agreement. The current world average \( B(B^+ \rightarrow \tau^+ \nu_\tau) = (1.14 \pm 0.27) \times 10^{-4} \) [6] shows no sign of physics beyond the SM. This average is obtained inflating the uncertainties of the input values by a factor of 1.22 to take into account discrepancies between the recent measurements.

The measurement described in this paper is performed using the final Belle data sample consisting of an integrated luminosity of 711 fb\(^{-1}\) containing \((772 \pm 11) \times 10^{6} BB\) pairs, collected at the \( \Upsilon(4S) \) resonance at the KEKB asymmetric-energy \( e^+ e^- \) collider [3]. We also use a smaller data sample with an integrated luminosity of 79 fb\(^{-1}\) taken at an energy lower than the \( \Upsilon(4S) \) mass to study the background from continuum \( e^+ e^- \rightarrow q\bar{q} (q = u, d, s, c) \) events and other processes without b-quark production. We generate multiple samples of simulated Monte Carlo (MC) events. We first simulate the decays to the final state using the software packageEvtGen [6], and then the interaction with the detector and its response using GEANT3 [11]. The simulated signal events are overlaid by beam related background, which was recorded with a random trigger.

The Belle detector is a large-solid-angle magnetic spectrometer that consists of a silicon vertex detector, a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter composed of CsI(Tl) crystals (ECL) located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux-return located outside the coil is instrumented to detect \( K_l^0 \) mesons and to identify muons (KLM). The detector is described in detail elsewhere [11]. Two inner detector configurations were used. A 2.0 cm beam-pipe and a 3-layer silicon vertex detector were used for the first sample of 152 \times 10^{6} BB pairs, while a 1.5 cm beam-pipe, a 4-layer silicon detector and a small-cell inner drift chamber were used to record the remaining 620 \times 10^{6} BB pairs [12].

Since the detectable signature of a \( B^+ \rightarrow \tau^+ \nu_\tau \) decay is often only a single charged track, we reconstruct the accompanying \( B \) meson (referred to as \( B_{tag} \)) in the semileptonic decay channels \( B^+ \rightarrow D^0 \ell^+ \nu_\ell \) and \( B^+ \rightarrow D^0 \ell^- \bar{\nu}_\ell \), where \( \ell \) can be an electron or muon. The \( D^0 \) mesons are reconstructed as \( D^0 \rightarrow D^0 \pi^0 \) and \( D^{*0} \rightarrow D^{*0} \gamma \) and the \( D^0 \) mesons as \( D^0 \rightarrow K^+ \pi^- \), \( K^- \pi^+ \), \( \rho^0 \pi^+ \pi^- \), \( K^0_{S} \pi^+ \pi^- \), \( K^0_{S} K^+ K^- \), and \( \pi^+ \pi^- \). Neutral pions are reconstructed as \( \pi^0 \rightarrow \gamma \gamma \) and \( K_S^0 \rightarrow \pi^+ \pi^- \).

To maximize the efficiency in reconstructing \( B_{tag} \) candidates, only loose requirements are applied. Charged final state particles are selected from well-measured tracks and are required to have a distance to the interaction point along (perpendicular to) the beam direction, further denoted as \( dz(dr) \), of less than 4 (2) cm. Photons used for the reconstruction of neutral pions are required to have an energy of at least 30 MeV and the invariant mass of the two-photon system must satisfy \( |M_{\gamma \gamma} - m_{\pi^0}| < 19 \text{ MeV}/c^2 \); this corresponds to a width of 3.2\( \sigma \). The invariant mass of the two charged tracks which are used to form \( K_S^0 \) candidates must lie within 30 MeV/c\(^2\) (4.5\( \sigma \)) of the nominal \( K_S^0 \) mass. The momenta of \( D^{(*)0} \) meson candidates are required to be below 2.5 GeV/c. All further selection is performed by training a multivariate selection (MVS) method, based on the NeuroBayes package [13]. A large sample of generically decaying simulated \( B \) mesons is used for this training and a broad range of information is considered in each stage of the reconstruction. Commonly used information is the mass, momentum, and decay channel of the particle candidate, as well as momenta, angles, and the output of the MVS of daughter particles. The structure of this semileptonic reconstruction method is very similar to the existing hadronic full reconstruction method [14]. The variables were chosen to be uncorrelated to the cosine of the angle between the momentum of the \( B \) meson and the \( D^{(*)}\ell \) system, calculated under the assumption that only one massless particle is not reconstructed. It is given by

\[
\cos \theta_{B,D^{(*)}\ell} = \frac{2E_{\text{beam}}E_{D^{(*)}\ell} - m_B^2 - m_{D^{(*)}\ell}^2}{2p_B^*p_{D^{(*)}\ell}^*},
\]

where \( E_{\text{beam}} \) is the energy of the beam in the center-of-mass system (CMS), \( E_{D^{(*)}\ell} \), \( m_B^2 \) and \( p_{D^{(*)}\ell}^* \) are the energy, mass and momentum of the \( (D^{(*)}\ell) \) system in the CMS, respectively, \( m_B \) is the nominal \( B \) meson mass [5], and \( p_B^* \) is the nominal \( B \) meson momentum in the CMS, calculated from the beam energy and the nominal mass. This angle is used later for further selection, since correctly reconstructed \( B_{tag} \) candidates have values between \(-1 \) and \(1\), while background events, where the assumption of only one missing massless particle does not hold, have a much larger range of values. Partially reconstructed \( B_{tag} \) candidates where only the slow pion or soft photon is not reconstructed lie in a broader range, but still peak around the signal region.

The \( B_{tag} \) candidates are combined with \( B \) mesons reconstructed in the decay mode \( B^+ \rightarrow \tau^+ \nu_\tau \), further denoted as \( B_{sig} \). The \( \tau \) lepton is reconstructed as \( \tau^+ \rightarrow \mu^+ \nu_\mu \), and \( e^+ \nu_e \), \( \pi^+ \nu_\pi \), and \( p^+ \bar{\nu}_p \), where the \( p^+ \) is reconstructed as \( p^+ \rightarrow \pi^+ \pi^0 \). Since the neutrinos cannot be detected, the \( B_{sig} \) candidate consists only of a single charged track or a \( p^+ \) candidate. The \( \rho^+ \) candidate is required to have an invariant mass within of 195 MeV/c\(^2\) of the nominal \( \rho^+ \) mass. The signal side particles are separated based on particle identification variables. The pion and kaon separation uses information from the ACC, TOF, and the \( dE/dx \) measurement in the CDC; the electron identification is based on the same information in addition to the shape of the shower and the energy measurement in the ECL; and muon candidates are identified using hits in the KLM matched to a charged track. The selection is performed such that signal side particle(s) can only be reconstructed in one of the potential particle hypotheses. The momentum of the signal side particle...
(e^+, \mu^+, \pi^+, \text{ or } \rho^+) \text{ in the CMS (}p_{\text{sig}}^*\text{) must be in the range } 0.5 \text{ GeV/c} < p_{\text{sig}}^* < 2.4 \text{ GeV/c.}

The combination of a B_{\text{tag}} \text{ and a } B_{\text{sig}} \text{ candidate is identical to the reconstruction of the } \Upsilon(4S). \text{ Since the } \Upsilon(4S) \text{ is produced without any accompanying particles, this allows for a powerful form of selection: we therefore reject events with additional } \pi^0 \text{ candidates or charged tracks with } |d| < 100 \text{ cm and } |dr| < 20 \text{ cm. In the decay channel } \tau^+ \rightarrow e^+\bar{\nu}_e, \text{ a significant background arises from events containing converted photons. To suppress this, we combine the electron, either the one used in the reconstruction of the } B_{\text{tag}} \text{ candidate or the one in the signal side, with every other oppositely charged track in the event. Using the electron mass hypothesis for the unspcic track, we require the invariant mass of the electron-track pair to be greater than 200 \text{ MeV/c}^2 \text{ for any of the pairs.}

To suppress background from continuum events, we train another MVS with the following input variables: the polar angle of the } B_{\text{tag}} \text{ candidate with respect to the beam direction in the CMS; the polar angle between the thrust axis of the } B_{\text{tag}} \text{ candidate and the remaining tracks in the event in the CMS; 16 modified FoxWolfram moments } \text{ and the momentum flow in nine concentric cones around the thrust axis of the } B_{\text{tag}} \text{ candidate } \text{. The requirement on the output of the MVS depends on the } \tau \text{ decay channel since the continuum background contribution differs significantly between them. The selection on } \cos\theta_{B,D_{\ell}\ell\tau} \text{ also differs between the } \tau \text{ decay channels. It is required to be smaller than 1 in all channels, but the lower limits are } -1.7, -1.9, -1.3, \text{ and } -2.6 \text{ for the muon, electron, pion, and } \rho \text{ final state, respectively. The selection is optimized using samples of simulated signal and background events to give the highest Figure of Merit } N_S/\sqrt{N_S+N_B}, \text{ where } N_S \text{ and } N_B \text{ are the number of selected signal and background events, respectively.}

We additionally perform a selection in the remaining energy in the ECL, further denoted as } E_{\text{ECL}}. \text{ It is defined as the sum of the energies of clusters in the ECL that are not associated to a final state particle of the reconstructed } \Upsilon(4S) \text{ candidate. To mitigate beam induced background in the energy sum, only clusters satisfying minimum energy thresholds of 50, 100, and 150 MeV are required for the barrel, forward, and backward end-cap calorimeter, respectively. Signal events peak near low values of } E_{\text{ECL}} \text{ as only photons from beam related background and misreconstructed events contribute, while the background is distributed over a much wider range. We require } E_{\text{ECL}} \text{ to be smaller than 1.2 GeV. The fraction of events with multiple signal candidates is 7%. In events with multiple candidates we choose the candidate with a maximal value of the tag side MVS classifier output. From MC simulation we find that this method selects the best candidate 70% of the time. The selection gives a total reconstruction efficiency of } \epsilon = (23.1 \pm 0.1) \times 10^{-4}, \text{ where the uncertainty is due to MC statistics only. It is described in detail in Table I.}

To study possible differences between real and simulated data, we use samples where the } B_{\text{sig}} \text{ is reconstructed in the decays } B^+ \rightarrow D^{0}\ell\nu_{\ell} \text{ and } B^+ \rightarrow D^0\pi^+ \text{ (further denoted as double-tagged samples). The } D^0 \text{ mesons are reconstructed as } D^{0} \rightarrow D^0\pi^0 \text{ and } D^{0} \rightarrow D^0\gamma \text{ and the } D^0 \text{ meson as } D^0 \rightarrow K^-\pi^+. \text{ The } D^* \text{ and } D \text{ meson candidates are selected based on their mass and the mass difference between the } D^* \text{ and the } D \text{ meson candidate. All selection related to the } B_{\text{tag}} \text{ and the event-wide vetoes are applied in addition to the signal side selection. There is a set of selection criteria for each of the } \tau \text{ decay channels. We apply each of these sets of selection criteria on each of the double-tagged samples, thus produce four samples for every } B \text{ decay channel, which only differ in the tag-side related selection. We measure the branching fractions of the } B \text{ decays and compare them to the current world averages } [2]. \text{ The reconstruction efficiency is corrected based on this ratio, depending on the decay channel of the } B_{\text{tag}} \text{ and the } \tau. \text{ The reconstruction efficiency is found to be overestimated by a factor of 1.02 to 1.18 in MC simulation.}

To extract the number of reconstructed signal events, we perform an extended two-dimensional unbinned maximum-likelihood fit in } p_{\text{sig}}^* \text{ and } E_{\text{ECL}}. \text{ We use smoothed histogram probability density functions (PDFs) } [17] \text{ obtained from MC to describe the signal and background components arising from events containing a } B\bar{B} \text{ pair. We use the product of one-dimensional PDFs for all components except for the signal in } \tau^+ \rightarrow \pi^+\bar{\nu}_\tau \text{ and } \tau^+ \rightarrow \rho^+\bar{\nu}_\tau \text{. In these modes the significant amount of cross-feed from other decay channels with additional, undetected neutral pions leads to a correlation between the } D^* \text{ and the } D \text{ meson candidate. All selection related to the } B_{\text{tag}} \text{ and the event-wide vetoes are applied in addition to the signal side selection. There is a set of selection criteria for each of the } \tau \text{ decay channels. We apply each of these sets of selection criteria on each of the double-tagged samples, thus produce four samples for every } B \text{ decay channel, which only differ in the tag-side related selection. We measure the branching fractions of the } B \text{ decays and compare them to the current world averages } [2]. \text{ The reconstruction efficiency is corrected based on this ratio, depending on the decay channel of the } B_{\text{tag}} \text{ and the } \tau. \text{ The reconstruction efficiency is found to be overestimated by a factor of 1.02 to 1.18 in MC simulation.}

| Final State | $e^+\nu_e\bar{\nu}_e$ | $\mu^+\nu_\mu\bar{\nu}_\mu$ | $\pi^+\bar{\nu}_\pi$ | $\pi^0\bar{\nu}_{\pi^0}$ |
|-------------|-------------------|------------------|-----------------|-------------------|
| $e^+\nu_e\bar{\nu}_e$ | 6.6 $\pm$ 0.1 | 0.1 $\pm$ 0.0 | 0.2 $\pm$ 0.0 | 0.1 $\pm$ 0.0 |
| $\mu^+\nu_\mu\bar{\nu}_\mu$ | 0.1 $\pm$ 0.0 | 4.7 $\pm$ 0.1 | 0.6 $\pm$ 0.0 | 0.2 $\pm$ 0.0 |
| $\pi^+\bar{\nu}_\pi$ | 0 | 0.1 $\pm$ 0.0 | 1.6 $\pm$ 0.0 | 0.5 $\pm$ 0.0 |
| $\pi^0\bar{\nu}_{\pi^0}$ | 0 | 0.1 $\pm$ 0.0 | 1.4 $\pm$ 0.0 | 4.9 $\pm$ 0.1 |
| Other | 0 | 0 | 0.2 $\pm$ 0.0 | 1.3 $\pm$ 0.0 |
| All | 6.8 $\pm$ 0.1 | 5.1 $\pm$ 0.1 | 4.0 $\pm$ 0.0 | 7.2 $\pm$ 0.1 |
| Total | 23.1 $\pm$ 0.1 |
ers, e.g., $\cos \theta_{p_{\mu}p_{\tau}}$, the outputs of the MVSs, and the missing energy in the event, by examining various control samples including the validation of the signal distribution in $E_{\mathrm{ECL}}$ and $p_{\text{sig}}$ using the double-tagged sample, which reveals no significant discrepancy between data and MC. The following five parameters are floated in the fit to the data to determine the signal branching fraction: $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$ and the normalization of the background in each of the $\tau$ decay channels. The relative signal yields in the $\tau$ decay channels are constrained by the ratios of the reconstruction efficiencies. Figure 1 shows the $E_{\mathrm{ECL}}$ distribution and Fig. 2 shows the $p_{\text{sig}}$ distribution projected in the region $E_{\mathrm{ECL}} < 0.2$ GeV. We obtain a total signal yield of $N_{\text{sig}} = 222 \pm 50$. This results in a branching fraction of $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) = (1.25 \pm 0.28) \times 10^{-4}$. The signal yields and branching fractions, obtained from fits for each of the $\tau$ decay modes separately are given in Table II.

![Fig. 1: Distribution of $E_{\mathrm{ECL}}$ for (a) $\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$, (b) $\tau^+ \rightarrow e^+ \bar{\nu}_e \nu_e$, (c) $\tau^+ \rightarrow \pi^+ \bar{\nu}_\pi$, and (d) $\tau^+ \rightarrow \rho^+ \bar{\nu}_\rho$. The markers show the data distribution, the solid line the total fitted distribution, and the dashed line the signal component. The orange (red) filled distribution represents the $BB$ (continuum) background.](image)

![Fig. 2: Distribution of $p_{\text{sig}}$, projected in the region $E_{\mathrm{ECL}} < 0.2$ GeV for (a) $\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$, (b) $\tau^+ \rightarrow e^+ \bar{\nu}_e \nu_e$, (c) $\tau^+ \rightarrow \pi^+ \bar{\nu}_\pi$, and (d) $\tau^+ \rightarrow \rho^+ \bar{\nu}_\rho$. The markers show the data distribution, the solid line the total fitted distribution, and the dashed line the signal component. The orange (red) filled distribution represents the $BB$ (continuum) background.](image)

| Decay Mode         | $N_{\text{sig}}$ | $B(10^{-4})$ |
|--------------------|------------------|--------------|
| $\tau^+ \rightarrow \mu^+ \bar{\nu}_\tau \nu_\mu$ | $134\pm21$ | $0.34\pm0.55$ |
| $\tau^+ \rightarrow e^+ \bar{\nu}_e \nu_e$       | $47\pm25$    | $0.90\pm0.47$ |
| $\tau^+ \rightarrow \pi^+ \bar{\nu}_\pi$         | $57\pm21$    | $1.82\pm0.68$ |
| $\tau^+ \rightarrow \rho^+ \bar{\nu}_\rho$        | $119\pm33$   | $2.16\pm0.60$ |
| Combined           | $222\pm50$     | $1.25\pm0.28$ |

TABLE II. Signal yields and branching fractions, obtained from fits for the $\tau$ decay modes separately and combined.

The list of systematic errors is given in Table III. The following systematic errors are determined by varying the corresponding parameters by their uncertainty, repeating the fit and taking the difference to the nominal fit result as systematic error: The normalization and slope of the continuum background component; the signal reconstruction efficiency; the branching fractions of dominant background decays, e.g. $B^- \rightarrow D^0 \ell^+ \nu_\ell$ followed by $D^0 \rightarrow K_L K_L$ or $D^0 \rightarrow K_L K_L K_L$; the correction of the tagging efficiency; obtained from the double tagged samples; and the branching fractions of the $\tau$ lepton. To estimate the effect of the uncertainty on the shape of the histogram PDFs due to the statistical uncertainty in the MC data, the content of each bin is varied following a Poisson distribution with the original content as mean before the fit is performed. This is repeated 1000 times and the width of the distribution of branching fractions is taken as systematic error. For the systematic related to the best candidate selection, we perform the selection and the fit without applying the best candidate selection, thus allowing for multiple candidates per event. The result is divided by the average multiplicity of 1.07 and compared to the nominal fit result. The uncertainty on the efficiency of the reconstruction of charged tracks and neutral pions and on the efficiency of the particle identification have been estimated using high statistics control samples. The charged track veto has been tested using the $D^0 \pi^+$ double-tagged sample by comparing the number of additional charged tracks in MC and data events. We find, that it agrees well, so we take the relative uncertainty on the number as systematic error. We also test an alternative description of the continuum background in $E_{\mathrm{ECL}}$ by using a polynomial of second order, but the deviation is well covered by the related systematic error, so we do not include it separately. The quadratic sum of all contributions is 22.0%.

We exclude the hypotheses of no $B^+ \rightarrow \tau^+ \nu_\tau$ decays with a significance of 3.8$\sigma$, by the convolution of the likelihood curve with a Gaussian distribution with a width of the systematic error. The significance is given by $\sqrt{2 \ln(\mathcal{L}/\mathcal{L}_0)}$, where $\mathcal{L}_0$ is the likelihood of the hy-
TABLE III. List of systematic errors.

| Source                                      | Relative Uncertainty (%) |
|---------------------------------------------|--------------------------|
| Histogram PDF shapes                        | 8.5                      |
| Continuum description                      | 14.1                     |
| Signal reconstruction efficiency           | 0.6                      |
| Background reconstruction efficiency       | 3.1                      |
| Efficiency calibration                     | 12.6                     |
| \(\tau\) decay branching fractions        | 0.2                      |
| Best candidate selection                   | 0.4                      |
| Charged track reconstruction               | 0.4                      |
| \(\pi^0\) reconstruction                  | 1.1                      |
| Particle identification                     | 0.5                      |
| Charged track veto                          | 1.9                      |
| Number of \(BB\) pairs                     | 1.4                      |
| Total                                       | 22.0                     |

In summary, we report the measurement of the branching fraction of \(B^+ \to \tau^+ \nu_\tau\) decays using a sample of \(772 \times 10^6 \B\B\) pairs, which we analyzed with the semileptonic tagging method. We measure it to be

\[ B(B^+ \to \tau^+ \nu_\tau) = [1.25 \pm 0.28{\text{(stat.)}} \pm 0.27{\text{(syst.)}}] \times 10^{-4} \]

with a significance of 3.8\( \sigma \). This result supersedes the previous measurement of the Belle collaboration \[5\]. It is consistent with previous measurements and with the SM expectation. We plan to combine this result with the recent measurement of the Belle collaboration using hadronic tagging \[6\] taking into account all relevant correlations of systematic errors.

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[1] Throughout this paper, the inclusion of the charge-conjugate decay mode is implied unless otherwise stated.
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