Statistical Analysis of Electricity Generation in Nigeria Using Multiple Linear Regression Model and Box-Jenkins’ Autoregressive Model of Order 1

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To cite this article:
Imo Enoidem Ebukanson, Chukwu Benedict Chidi, Abode Innocent Iriaoghuan. Statistical Analysis of Electricity Generation in Nigeria Using Multiple Linear Regression Model and Box-Jenkins’ Autoregressive Model of Order 1. International Journal of Energy and Power Engineering. Vol. 6, No. 3, 2017, pp. 28-33. doi: 10.11648/j.ijepe.20170603.12

Received: January 8, 2017; Accepted: January 18, 2017; Published: June 7, 2017

Abstract: This study presents statistical analysis of electricity generation in Nigeria using two different statistical models, namely; multiple linear regression model and box-Jenkins’ autoregressive model of order 1. Two climatic variables (rainfall and temperature) were used as the explanatory variables. Data on electricity generation in Nigeria between 2002 and 2014 were obtained from the Central Bank of Nigeria Statistical Bulletin while Data on rainfall and temperature between 2002 and 2014 were extracted from the National Bureau of Statistics (NBS) abstract. Test of model fitness and forecasting accuracy were done using generic statistical approach which include coefficient of determination and root mean square error. The prediction accuracy of the two statistical models was compared and the best model was selected. Furthermore, correlation between power generation and the two climatic variables (rainfall and temperature), were carried out and the result reveals that the amount of rainfall has significant and positive relationship with power generation in Nigeria. Specifically, rainfall has correlation value of r = 0.927 with the power generation at probability, p = 0.000 and the relationship was significant at 1% (p<0.01). However, temperature although it is positively correlated, does not significantly affect power generation. Temperature has correlation value of r = 0.136 with power generation at probability, p = 0.658 (p>0.05) and the relationship was significant at 5% (p<0.05). Among the two statistical models, multiple linear regression model was selected as the best model as it gave the highest value of coefficient of determination (r²=99.77%) and the least Root Mean Square Error (60.27%).

Keywords: Electricity, Box-Jenkins’ Autoregressive Model, Electricity Generation, Multiple Linear Regression Model, Statistical Analysis of Electricity

1. Introduction

Electricity generation and supply is indispensable in modern living in any industrial or commercial society. Electricity production in Nigeria over the years varied from gas – fired, oil – fired, hydroelectric power stations to coal-fired with hydroelectric power system and gas – fired system taking precedence [1-4]. Presently, Nigeria mostly employs gas-fired and hydroelectric turbines for bulk generation, oil being too expensive and coal-fired stations having gone moribund.

Nigeria being rapidly growing in development, industry and commerce, is battling with the problems of continually expanding consumption and increase in demand for electricity. Madueme [5] observed that in Nigeria, the national peak demand for electric energy is on the increase as a result of many development activities. He went further to state that in spite of this, the total power generation has not matched this increase. It is a fact that most communities in Nigeria regard the construction of access roads, installation of pipe borne water, building of town halls and so forth as the rudiments to their development, yet electricity promotes instantly their social and economic life as many services and facilities become readily available [6].
In this regard, adequate electricity generation constitute a central development issue which cannot be over-emphasized [7-11]. Apart from serving as the pillar of wealth creation in Nigeria, it is also the nucleus of operations and subsequently the engine of growth for all sectors of the economy. This study examines how the power generation will be affected by climate change or variables such as temperature and rainfall which is regarded as one of the greatest threat to humanity in the 21st century. Considerable efforts have been made in assessing the causal link between energy consumption and economic growth, but very few studies have examined how environmental challenges such as the incidence of climate change will significantly impact energy production which is regarded as the bane of economic growth. Most researches in the aspect of impacts of climate change on the energy sector are in form of technical reports; some others examine how the energy sector contributes to climate change and not so much on how the energy sector will be affected by the incidence of climate change. This study will attempt to fill this gap in addition to examining the bivariate relationship between two climate variables (rainfall and temperature) and electric power generation in Nigeria between 2002 and 2014, conducting statistical analysis of electric power generation in Nigeria between 2002 and 2014, extracting data on rainfall and temperature and electric power generation in Nigeria between 2002 and 2014 were obtained from the Central Bank of Nigeria statistical bulletin [20].

Data on electricity generation in Nigeria between 2002 and 2014 were extracted from the National Bureau of Statistics (NBS) abstract [21].

2. Methodology

In this study, analytical and simulation research methodologies are used. In the analytical method, statistical models are developed for analysing and predicting electricity generation in Nigeria. Specifically, two different statistical models are used in this study. These models are multiple linear regression model [12-14] and Box-Jenkins’ autoregressive model of order 1 [15-19]. It also provides the source and method of data collection.

2.1. Source and Method of Data Collection

The source of data collection for this study is secondary. Data on electricity generation in Nigeria between 2002 and 2014 were obtained from the Central Bank of Nigeria statistical bulletin [20] while data on rainfall and temperature were extracted from the National Bureau of Statistics (NBS) abstract [21].

2.2. Multiple Linear Regression

The multiple linear regression can be represented mathematically as:

\[ G_i = \beta_0 + \beta_1 R_i + \beta_2 T_i + \epsilon_i \]  \hspace{1cm} (1)

Making the residual the subject in equation (1) gives:

\[ \epsilon_i = G_i - \beta_0 - \beta_1 R_i - \beta_2 T_i \]  \hspace{1cm} (2)

The sum of square error (S_2) is given as:

\[ S_2 = \sum_{n=1}^{n} (G_i - \beta_0 - \beta_1 R_i - \beta_2 T_i)^2 \]  \hspace{1cm} (3)

\[ \frac{\partial S_2}{\partial \beta_0} = 2(-1) \sum_{n=1}^{n} (G_i - \beta_0 - \beta_1 R_i - \beta_2 T_i) = 0 \]  \hspace{1cm} (4)

\[ \frac{\partial S_2}{\partial \beta_1} = 2(-1) \sum_{n=1}^{n} [R_i (G_i - \beta_0 - \beta_1 R_i - \beta_2 T_i)] = 0 \]  \hspace{1cm} (5)

\[ = 2(-1) \sum_{n=1}^{n} [R_i G_i - \beta_0 R_i - \beta_1 R_i^2 - \beta_2 R_i T_i] \]

\[ \frac{\partial S_2}{\partial \beta_2} = -2 \sum_{n=1}^{n} T_i (G_i - \beta_0 - \beta_1 R_i - \beta_2 T_i) = 0 \]  \hspace{1cm} (6)

To find estimate of the parameters \((\beta_0, \beta_1, \beta_2)\), equations (3), (5), (6) are set to zero. Then,

\[ \sum_{n=1}^{n} G_i - n\beta_0 - \beta_1 \sum_{n=1}^{n} R_i - \beta_2 \sum_{n=1}^{n} T_i = 0 \]  \hspace{1cm} (7)

\[ \sum_{n=1}^{n} R_i G_i - \beta_0 \sum_{n=1}^{n} R_i - \beta_1 \sum_{n=1}^{n} R_i^2 - \beta_2 \sum_{n=1}^{n} R_i T_i = 0 \]  \hspace{1cm} (8)

\[ \sum_{n=1}^{n} T_i G_i - \beta_0 \sum_{n=1}^{n} T_i - \beta_1 \sum_{n=1}^{n} T_i R_i - \beta_2 \sum_{n=1}^{n} T_i^2 = 0 \]  \hspace{1cm} (9)

Rearranging equations (7), (8) and (9) gives:

\[ n\beta_0 + \beta_1 \sum_{n=1}^{n} R_i + \beta_2 \sum_{n=1}^{n} T_i = \sum_{n=1}^{n} G_i \]  \hspace{1cm} (10)

\[ \beta_0 \sum_{n=1}^{n} R_i + \beta_1 \sum_{n=1}^{n} R_i^2 + \beta_2 \sum_{n=1}^{n} R_i T_i = \sum_{n=1}^{n} R_i G_i \]  \hspace{1cm} (11)

\[ \beta_0 \sum_{n=1}^{n} T_i + \beta_1 \sum_{n=1}^{n} T_i R_i + \beta_2 \sum_{n=1}^{n} T_i^2 = \sum_{n=1}^{n} T_i G_i \]  \hspace{1cm} (12)

Solving the systems of the equations, 10 to 12, give the estimate of the parameters of the model.

2.3. Box Jenkins’ Autoregressive Model of Order 1

The Box Jenkins’ Autoregressive Model of Order 1 can be expressed mathematically in the form:

\[ g_t = \gamma_0 + \gamma_{g,t-1} + \epsilon_t \]  \hspace{1cm} (13)

The residual term \( \epsilon_t \) can be obtained from Equation (12) as:

\[ \epsilon_t = g_t - (\gamma_0 + \gamma_{g,t-1}) \]  \hspace{1cm} (14)

\[ \epsilon_t = (g_t - \gamma_0 - \gamma_{g,t-1}) \]  \hspace{1cm} (15)
The sum of square error can be expressed as:

$$S_d = \sum_{i=1}^{n} e_i^2 = \sum_{i=1}^{n} (G_i - \gamma \hat{G}_i)^2$$  \hspace{1cm} (16)

Differentiating the Equation (16) with respect to $\gamma_0, \gamma_1$

$$\frac{\partial S_d}{\partial \gamma_0} = -2\sum_{i=1}^{n} (G_i - \gamma_0 \hat{G}_i)$$  \hspace{1cm} (17)

$$\frac{\partial S_d}{\partial \gamma_1} = -2\sum_{i=1}^{n} \hat{G}_i (G_i - \gamma_0 \hat{G}_i)$$  \hspace{1cm} (18)

$$\frac{\partial S_d}{\partial \gamma_1} = -2\left[ \sum_{i=1}^{n} G_i \hat{G}_i - \gamma_0 \sum_{i=1}^{n} \hat{G}_i - \gamma_1 \sum_{i=1}^{n} G_i^2 \right]$$  \hspace{1cm} (19)

To obtain the parameters ($\gamma_0, \gamma_1$) we set the partial derivation with respect to each parameter to 0. Then:

$$n\gamma_0 + \gamma_0 \sum_{i=1}^{n} G_i - \gamma_1 \hat{G}_i = \sum_{i=1}^{n} G_i$$  \hspace{1cm} (20)

$$\gamma_0 \sum_{i=1}^{n} \hat{G}_i + \gamma_1 \sum_{i=1}^{n} G_i - \gamma_1 \sum_{i=1}^{n} G_i \hat{G}_i = \sum_{i=1}^{n} G_i \hat{G}_i$$  \hspace{1cm} (21)

Solving the set of equations 20-21, with two unknowns ($\gamma_0, \gamma_1$), this will give the estimates of the model parameters.

### 2.4. Test of Model Fitness

#### 2.4.1. Coefficient of Determination

SST is the sum of square total which is given as:

$$SST = \sum_{i=1}^{n} (G_i - \bar{G})^2$$  \hspace{1cm} (22)

Where $G_i$ is the electricity generated during the year

$$SS \ (Error) = \sum_{i=1}^{n} (G_i - \hat{G})^2$$  \hspace{1cm} (23)

$$SS \ (Regression) = \sum_{i=1}^{n} (\hat{G}_i - \bar{G})^2$$  \hspace{1cm} (24)

Coefficient of Determination ($r^2$) is given as:

$$r^2 = \frac{SSR}{SST}$$  \hspace{1cm} (25)

Where $\bar{G}$ and $\hat{G}$ are the mean and estimated electricity generation.

#### 2.4.2. Root Mean Square Error (RMSE)

The root mean square error was used to assess the forecasting accuracy of the four models. The RMSE is defined as:

$$RMSE = \sqrt{MSE}$$  \hspace{1cm} (26)

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (G_i - \hat{G}_i)^2$$  \hspace{1cm} (27)

Where $G_i$ and $\hat{G}_i$ are the electricity generated during the year and estimated electricity generation and $n$ is the number of observation.

### 3. Results and Discussion

The data on electricity generation obtained from central bank of Nigeria statistical bulletin and the two climatic variables (rainfall and temperature) extracted from National Bureau of statistics abstract between 2002 and 2014 were analysed based on the two different statistical models. Correlation between power generation and climatic variables was carried out. Graphpad prism 5.0 Econometric View (E-View) software was used to plot the graph of actual and predicted power generation in Nigeria between 2002 and 2014 for the two statistical models. Generic statistical approach was used to assess the goodness of fit and forecasting accuracy of the two models. The prediction accuracy of the two models was compared and the best model was selected.

Table 1 shows the result of bivariate relationship between power generation and the climatic variables. The result reveals that the amount of rainfall was found to be significantly related with power generation ($r = 0.927$, $p = 0.000$, $p<0.01$). The relationship was significantly positive which means that as the amount of rainfall increases, power generation also increases. Also, the relationship between the temperature and power generation was also positive but not significant ($t = 0.136$, $p = 0.658$, $p>0.05$). This relationship was not significant at 5 percent ($p<0.05$).

| G   | R    | T    |
|-----|------|------|
| G   | 1    |      |
| R   | 0.927 (0.000) | 1    |
| T   | 0.136 (0.658) | -0.117 (0.703) | 1 |

$G$ = Power generation, $R$ = rainfall, $T$ = temperature. *Significant at 1% ($p<0.01$), *significant at 5% ($p<0.05$).

#### 3.1. Multiple Linear Regression

Table 2 shows that the parameters of the multiple linear regression are as follows:

$$\beta_0 = -2609.781, \ \beta_1 = 0.4600, \ \beta_2 = 136.1937.$$  \hspace{1cm}

Therefore, the estimated model for power generation based on the multiple linear regression is:

$$G = -2609.781 +0.4600 R+ 136.1937T$$  \hspace{1cm} (28)

The coefficient of determination is 0.9977. This indicates that rainfall and temperature explained for 99.77% of the variation in power generation while the remaining 0.23
percent of the variation in power generation could be due to other variables not accounted for in the multiple linear regression model. Furthermore, the coefficient of rainfall ($\beta = 0.46$) is positive meaning that as rainfall increases, power generation also increases.

Table 2. Summary result of the estimates of the multiple linear regression model.

| Model Parameters | $\beta$ | SSR        | SST          | $r$-square | RMSE (%) |
|------------------|--------|------------|--------------|------------|----------|
| Constant         | -2609.781 | 47229.207 | 20833613 0.9977 | 60.2745 |
| Rainfall         | 0.4600 |            |              |            |          |
| Temperature      | 136.1937 |            |              |            |          |

$\beta =$ coefficients, SSR = regression sum of square, SST = Total Sum of Square, RMSE = Root Mean Square Error.

3.2. Box Jenkins’s Autoregressive Model of Order 1

The Box’s Jenkin’s AR (1) model for power generation is:

$$G_t = 684.1545 + 0.770103G_{t-1}$$ (29)

From Table 4, Box Jenkin’s AR (1) model gave an $r^2$ value of 98.45% which means that the model explained 98.45 percent of the variation in power generation in Nigeria. The coefficient of power generation at one period lag ($\beta = 0.770103$) is positive which means that power generation will increase with time.

The Box’s Jenkin’s AR (1) model for power generation is:

$$G_t = 684.1545 + 0.770103G_{t-1}$$ (30)

From Table 4, Box Jenkin’s AR (1) model gave an $r^2$ value of 98.45% which means that the model explained 98.45 percent of the variation in power generation in Nigeria. The coefficient of power generation at one period lag ($\beta = 0.770103$) is positive which means that power generation will increase with time.

Table 3. Actual and Predicted power generation in Nigeria between 2002 and 2014 using multiple linear regression model.

| Year | Actual generation (MWh) | Predicted generation (MWh) |
|------|--------------------------|----------------------------|
| 2002 | 2564.3                   | 2577.93                    |
| 2003 | 2660.0                   | 2693.14                    |
| 2004 | 2663.6                   | 2624.14                    |
| 2005 | 2569.3                   | 2605.05                    |
| 2006 | 2871.3                   | 2866.97                    |
| 2007 | 2706.3                   | 2729.27                    |
| 2008 | 2698.1                   | 2726.33                    |
| 2009 | 2701.4                   | 2724.31                    |
| 2010 | 2703.5                   | 2717.15                    |
| 2011 | 2650.0                   | 2590.67                    |
| 2012 | 2719.9                   | 2732.22                    |
| 2013 | 3225.0                   | 3319.79                    |
| 2014 | 3249.0                   | 3080.48                    |

Table 4. Summary result of the estimates of the box Jenkin’s autoregressive model of order 1.

| Model Parameters | $\beta$ | SSR                  | SST                  | $r$-square | RMSE (%) |
|------------------|--------|----------------------|----------------------|------------|----------|
| Constant         | 684.1545 | 21827609.17 22170749.38 | 0.9845 169.1006 |            |          |
| $G_{t-1}$        | 0.770103 |            |              |            |          |

$\beta =$ coefficients, SSR = regression sum of square, SST = Total Sum of Square, RMSE = Root Mean Square Error.

Table 5. Actual and Predicted power generation in Nigeria between 2003 and 2014 using box Jenkin’s autoregressive model of order 1.

| Year | Actual generation (MWh) | Predicted generation (MWh) |
|------|--------------------------|----------------------------|
| 2003 | 2660.0                   | 2658.93                    |
| 2004 | 2663.6                   | 2732.63                    |
| 2005 | 2569.3                   | 2735.40                    |
| 2006 | 2871.3                   | 2662.78                    |
| 2007 | 2706.3                   | 2895.35                    |
| 2008 | 2698.1                   | 2768.28                    |
| 2009 | 2701.4                   | 2761.97                    |
| 2010 | 2703.5                   | 2764.51                    |
| 2011 | 2650.0                   | 2766.13                    |
| 2012 | 2719.9                   | 2724.93                    |
| 2013 | 3225.0                   | 3319.79                    |
| 2014 | 3249.0                   | 3080.48                    |
3.3. Comparison of the Forecasting Accuracy of the Two Models

Table 6. Comparison of the forecasting accuracy of the two models.

| S/N | Models                                  | r-square (%) | RMSE   | Rank |
|-----|-----------------------------------------|--------------|--------|------|
| 1   | Multiple linear regression              | 99.77        | 60.27  | 1    |
| 2   | Box-Jenkins’s Autoregressive Model of order 1 | 98.45        | 169.10 | 2    |

Based on the result in Table 6, the multiple linear regression model has the highest coefficient of determination (r-square = 99.77%) and least root mean square error (RMSE = 60.27). Hence, the multiple linear regression model is recommended as the best of the two competing models.

4. Conclusion

In this study, correlation between power generation and two climatic variables are presented. The result reveals that the amount of rainfall has significant and positive relationship with power generation in Nigeria. The relationship was significantly positive which means that as the amount of rainfall increases, power generation also increases. However, temperature although positive, does not significantly affect power generation. From the results obtained from model 1 shows that the two independent variables (rainfall and temperature) explained for 99.77% of the variation in electricity generation. The multiple linear regression model was selected as the best model as it gave the highest value of coefficient of determination ($r^2=99.77\%$) and the least root mean square error (60.27%).

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