In this manuscript, the theory of constant picture fuzzy graphs (CPFG) is developed. A CPFG is a generalization of constant intuitionistic fuzzy graph (CIFG) and a special case of picture fuzzy graph (PFG). Additionally, the article includes some basic definitions of CPFG such as totally constant picture fuzzy graphs (TCPFGs), constant function, bridge of CPFG, and their related results. Also, an application of CPFG in Wi-Fi network system is discussed. Finally, a comparison of CPFG is established with that of the CIFG which exhibits the superiority of the proposed idea over the existing ones is discussed.

1. Introduction

Wi-Fi systems and the analysis of their signals have been under discussion during the last decades [1, 2]. To provide signals effectively, potential research has been carried out in [3, 4]. A Wi-Fi device within the range can either be connected, disconnected, or fluctuate between the state of connected and disconnected or it could be out of range. Such uncertain situations can be dealt by the idea of PFG which proves to be helpful in such cases.

Zadeh [5] proposed the theory of fuzzy sets (FSs) that is very popular tool and is considered the superior tool till now. Kaufman defined fuzzy graph (FG) in [6]. A detailed study is contributed by Rosenfeld in his article [7]. Since then theory of FGs has been extensively applied to many fields such as clustering [8–10], networking [11, 12] and communication problems [13–15].

Atanassov [16] proposed intuitionistic fuzzy set (IFS) as a generalization of fuzzy set (FS). The concept of intuitionistic fuzzy relations has also been discussed in [16] providing fundamentals of the theory of IFGs. Parvathi and Karunambigai [17] defined IFGs as generalization of FGs and discussed various graph theoretic concepts. For detailed work in the course of IFGs, one may refer to [18–26]. The structure of IFGs is diverse than that of FGs and it is applied to many problems such as radio coverage networking [22], decision making and shortest path problems [20, 27–31], and social networks [32].

In Wi-Fi networks, we usually face more situations that we could not handle by FGs and IFGs. Therefore, in this article, the idea of PFG and consequently CPFG is introduced as a generalization of constant IFGs. The properties and results of CPFG are discussed and illustrated with examples. In addition, a Wi-Fi network problem is modeled using CPFGs.

The article starts with introduction followed by the section that discusses some basic ideas. The third section is based on concepts of PFGs while section four is based on CPFGs and its related theory. In section five, an application is discussed thoroughly with some numerical explanations. Finally, the concluding statements are added to the manuscript.

2. Preliminaries

This section discusses some basic ideas of graph theory including the ideas of FGs and IFGs. These concepts of FGs and IFGs are illustrated with the help of examples.
Definition 1 (see [7]). An FG is a pair $\tilde{G} = (V, \tilde{E})$ such that

1. $V$ is the set of vertices and $T_1, F_1$ maps on $[0, 1]$ are the association degree of $v_i \in V$.
2. $\tilde{E} = \{(v_i, v_j) : (v_i, v_j) \in V \times V\}$ and $T_2 : V \times V \rightarrow [0, 1]$, where $T_2(v_i, v_j) \leq \min\{T_1(v_i), T_1(v_j)\}$ for all $(v_i, v_j) \in \tilde{E}$.

Example 1. An FG $\tilde{G} = (V, \tilde{E})$ with the collection of vertices $V$ and the collection of edges $\tilde{E}$ is depicted in Figure 1.

Definition 2 (see [17]). An IFG is a pair $\tilde{G} = (V, \tilde{E})$ such that

1. $V$ is the set of vertices such that $T_1$ and $F_1$ maps on the closed interval $[0, 1]$ represent the grads of membership and nonmembership of the vertex elements $v_i \in V$, respectively, with a condition $0 \leq T_1 + F_1 \leq 1$ for all $v_i \in V$, $(i \in I)$.
2. $\tilde{E} \subseteq V \times V$ where $T_2, F_2 : V \times V \rightarrow [0, 1]$ represent the grads of membership and nonmembership of the edge elements $(v_i, v_j) \in \tilde{E}$ such that $T_2(v_i, v_j) \leq \min\{T_1(v_i), T_1(v_j)\}$ and $F_2(v_i, v_j) \leq \max\{F_1(v_i), F_1(v_j)\}$ with a condition $0 \leq T_2(v_i, v_j) + F_2(v_i, v_j) \leq 1$ for all $(v_i, v_j) \in \tilde{E}$, $(i \in I)$.

Example 2. Consider an IFG $\tilde{G} = (V, \tilde{E})$ depicted in Figure 2.

3. Picture Fuzzy Graphs

This section is based on some very basic concepts related to PFGs including its definition, and some of its associated terms such as degree of PFGs and completeness of PFGs are discussed.

Definition 3. A PFG is a pair $\tilde{G} = (V, \tilde{E})$ such that

1. $V$ is the collection of vertices such that $T_1, \Gamma_1, F_1 : V \rightarrow [0, 1]$ represent the grads of membership, abstinence, and nonmembership of the vertex elements $v_i \in V$, respectively, so long as $0 \leq T_1 + \Gamma_1 + F_1 \leq 1$ for all $v_i \in V$, $(i \in I)$.
2. $\tilde{E} \subseteq V \times V$ where $T_2, \Gamma_2, F_2 : V \times V \rightarrow [0, 1]$ represent the grads of membership, abstinence, and nonmembership of the edge elements $(v_i, v_j) \in \tilde{E}$ such that $T_2(v_i, v_j) \leq \min\{T_1(v_i), T_1(v_j)\}$, $\Gamma_2(v_i, v_j) \leq \min\{\Gamma_1(v_i), \Gamma_1(v_j)\}$, and $F_2(v_i, v_j) \leq \max\{F_1(v_i), F_1(v_j)\}$ as long as $0 \leq T_2(v_i, v_j) + \Gamma_2(v_i, v_j) \leq F_2(v_i, v_j) \leq 1$ for all $(v_i, v_j) \in \tilde{E}$, $(i \in I)$.

Moreover, $1 - (T_1 + \Gamma_1 + F_1)$ represent refusal degree.

Example 3. A PFG $\tilde{G} = (V, \tilde{E})$ is depicted in Figure 3.

Definition 4. Let $\tilde{G} = (V, \tilde{E})$ be PFG. Then, the degree of any vertex $v$ is defined by $d(v) = (d_T(v), d_F(v), d_{\bar{v}}(v))$, where

$$d_T(v) = \sum_{u \in V, T_2(v, u)} T_2(v, u)\text{, \hspace{1cm}} d_F(v) = \sum_{u \in V, F_2(v, u)} F_2(v, u)\text{, \hspace{1cm}} \text{and} \hspace{1cm} d_{\bar{v}}(v) = \sum_{u \in V, \bar{v}(v, u)} \bar{v}(v, u)\text{.}$$

Example 4. A PFG $\tilde{G} = (V, \tilde{E})$ depicted in Figure 4 is calculated as follows.

Degree of vertices is

$$d(v_1) = (0.3, 0.3, 0.8), \hspace{1cm} d(v_2) = (0.2, 0.3, 0.8), \hspace{1cm} d(v_3) = (0.0, 0.3, 0.8), \hspace{1cm} d(v_4) = (0.1, 0.3, 0.8).$$

Definition 5. The complement $\tilde{G}'$ of PFG $\tilde{G} = (V, \tilde{E})$ is as follows:

1. $T_1(v_i)’ = T_1(v_i), \Gamma_1(v_i)’ = \Gamma_1(v_i), F_1(v_i)’ = F_1(v_i), \forall v_i \in V.$
2. $T_2(v_i, v_j)’ = \min\{T_1(v_i), T_1(v_j)\}$, $\Gamma_2(v_i, v_j)’ = \min\{\Gamma_1(v_i), \Gamma_1(v_j)\}$, $F_2(v_i, v_j)’ = \max\{F_1(v_i), F_1(v_j)\}$, $\forall v_i, v_j \in E.$
Remark 1. According to definition of a compliment, for a PFG, $\tilde{G} = (V, \tilde{E})$, the graph $G'' = (V', \tilde{E}'' = \tilde{G}$.

Proposition 1. $\tilde{G} = G''$ $\Leftrightarrow G$ is a strong PFG.

Proof. According to the definition of $G''$, the result and the proof are straight forward.

Example 5. Figures 5 and 6 provide a verification of Proposition 1.

Definition 6. A PFG $\tilde{G}$ is called a self-complementary graph if $G = G''$.

Definition 7. A PFG is said to be a complete PFG if $T_2(v_i, v_j) = \min\{T_1(v_i), T_1(v_j)\}$,

$\tilde{T}_2(v_i, v_j) = \min\{\tilde{T}_1(v_i), \tilde{T}_1(v_j)\}$, and $F_2(v_i, v_j) = \max\{F_1(v_i), F_1(v_j)\}$.

Example 6. A complete PFG is depicted in Figure 7.

Definition 8. For any pair of different vertices $(v_i, v_j)$ in a PFG, $G = (V, \tilde{E})$, if deleting the edge $(v_i, v_j)$ lessens the strength between that pair of vertices, then this edge is called the bridge in graph $G$.

Example 7. A PFG $\tilde{G} = (V, \tilde{E})$ is depicted in Figure 8 and explained as follows.

In Figure 8, the strength of $v_1v_4$ is $(0.1, 0.3, 0.4)$. Since the removal of $(v_1, v_4)$ from $G$ lessens the strength between the vertices $v_1$ and $v_4$ in $G$, therefore, $(v_1, v_4)$ is a bridge.

Definition 9. For a PFG $G$, If we remove a vertex $v_i$ in $G$ which decreases the strength of connectedness among some pairs of vertices, then it is called cut vertex of $G$.

4. Constant Picture Fuzzy Graph

Definition 10. A PFG $\tilde{G} = \{(v_i, T_1, \tilde{T}_1, F_1), (k_i, T_2, \tilde{T}_2, F_2)\}$ is known as CPFG of degree $(k_i, k_j, k_k)$ or $(k_i, k_j, k_k) - \text{PFG}$. If

$$d_T(v_i) = k_i, \quad d_T(v_j) = k_j, \quad v_i, v_j \in V. \quad (2)$$

Example 8. A $\tilde{G} = (V, \tilde{E})$. Then, the CPFG is depicted in Figure 9.

Example 9. A complete PFG needs not be a CPFG depicted in Figure 10 and explained as follows.

Figure 8 clearly shows that it is a complete PFG but not constant.

Definition 11. The total degree $(\tau_1, \tau_2, \tau_3)$ of a vertex $v \in V$ in PFG $G$ is defined as
Theorem 1. \( \text{Example 10.} \)
\( \text{PFG of total degree 0.} \)

\[ \text{Figure 4: Journal of Mathematics} \]

\[ \text{Figure 7: (Complete PFG).} \]

\[ \text{Figure 8: (PFG).} \]

\[ \text{Figure 10: (Complete PFG).} \]

\[ \text{Figure 9: (CPFG).} \]

\[ \text{Figure 11: (Totally constant PFG).} \]

**Proof.** 
(i) \( \Leftrightarrow \) (ii) Consider \( (T_1, \Gamma_1, F_1) \) is a constant function. Suppose \( T_1(v_i) = c_1, \Gamma_1(v_i) = c_2 \) and \( F_1(v_i) = c_3 \forall v_i \in V \) where \( c_1, c_2, \) and \( c_3 \) are constants. Let \( G \) be a constant PFG. Then, \( d_T(v_i) = v_i, d_T(v_i) = v_2 \) and \( d_T(v_i) = k_1 \forall v_i \in V \). So, \( T_1(v_i) = d_T(v_i) + T_1(v_i), T_2(v_i) = d_T(v_i) + \Gamma_1(v_i) \) and \( F_1(v_i) = d_T(v_i) + F_1(v_i) \forall v_i \in V, d_T(v_i) = k_1 + c_1, \) \( d_T(v_i) = k_2 + c_2, \) \( d_T(v_i) = k_3 + c_3 \forall v_i \in V \). Hence, (ii) is proved. 

(ii) \( \Rightarrow \) (i) Assume that \( \bar{G} \) is a \((\tau_1, \tau_2, \tau_3)\)-TCPFG. Then, \( T_1(v_i) = \tau_1, d_T(v_i) = \tau_2 \) and \( d_T(v_i) = \tau_3 \forall v_i \in V \). (iii) is proved. 

(iii) \( \Rightarrow \) (ii) Assume that \( \bar{G} \) is a constant function iff \( (T_1, \Gamma_1, F_1) \) is a TCPFG. Assume that \( (T_1, \Gamma_1, F_1) \) is not a constant function. Then, \( T_1(v_i) \neq T_2(v_i), \Gamma_1(v_i) \neq \Gamma_2(v_i), F_1(v_i) \neq F_2(v_i) \forall v_i \in V \) and if \( \Gamma_1(v_i) \neq \Gamma_2(v_i) \) is a constant function, then \( T_1(v_i) = T_2(v_i) = k_1, \Gamma_1(v_i) = \Gamma_2(v_i) = k_2, F_1(v_i) = F_2(v_i) = k_3 \). So, \( d_T(v_i) = d_T(v_i) + T_1(v_i) = k_1 + T_1(v_i) \) and \( d_T(v_i) = k_1 + \Gamma_1(v_i) + \Gamma_2(v_i) = k_2 + F_1(v_i) \) and \( d_T(v_i) = k_3 + F_2(v_i) \). Hence, \( T_1(v_i) \neq T_2(v_i), \Gamma_1(v_i) \neq \Gamma_2(v_i) \neq \Gamma_3(v_i) \neq F_1(v_i) \neq F_2(v_i) \neq F_3(v_i) \). 

Example 10. Consider a TCPFG depicted in Figure 11.

**Theorem 1.** \( (T_1, \Gamma_1, F_1) \) is a constant function (CF) in a PFGG if and only if the following are equivalent:

(i) \( \bar{G} \) is a constant PFG.
(ii) \( \bar{G} \) is totally PFG.

\[ \square \]
Example 11. A PFG $G = (V, E)$ is CPFG and TCPFG. Figure 12 explains the defined concept.

Theorem 2. A constant and totally constant graph $\tilde{G}$ implies that $(T_1, \tilde{f}_1, F_1)$ is CF.

Proof. Suppose $\tilde{G}$ is CPFG and TCPFG. Then, $d_T(v_i) = k_1, d_T(v_i) = k_2$ and $d_T(v_i) = k_3$ and $d_T(v_i) = \tau_1, d_T(v_i) = \tau_2, d_T(v_i) = \tau_3$. As $d_T(v_i) = \tau_1$ where $v \in V$, then $d_T(v_i) = \tau_1, \forall v \in V$. $k_1 + T_1(v_i) = \tau_1, \forall v \in V$ implies $T_1(v_i) = \tau_1 - k_1, \forall v \in V$. Therefore, $\Gamma_1(v_i)$ is a constant function. Likewise, $\Gamma_1(v_i) = \tau_2 - k_2$ and $F_1(v_i) = \tau_3 - k_3, \forall v \in V$. \hfill $\Box$

Remark 2. Converse of the above theorem is not true in general.

Example 12. A PFG is not CPFG and not TCPFG. Figure 13 explains the defined concept.

Theorem 3. If a crisp graph $G$ is an odd cycle and $\tilde{G}$ is aPFG, then $G$ is CPFG $\Rightarrow (T_1, \tilde{f}_1, F_1)$ which is a CF.

Proof. Assume that $(T_2, \tilde{f}_2, F_2)$ is a constant function that implies $T_2 = c_1, T_2 = c_2, F_2 = c_3 \forall v_j, v_j \in \tilde{E}$, and implies $d_T(v_i) = 2c_1, d_T(v_i) = 2c_2, \text{and } d_T(v_i) = 2c_3$, for any $v_i \in \tilde{E}$, therefore, $G$ is a CPFG.

Consider $\tilde{G}$ is a $(k_1, k_2, k_3)$-regular PFG. Consider $\tilde{e}_1, \tilde{e}_2, \tilde{e}_3, \ldots, \tilde{e}_{n+1}$ represented the edges of $\tilde{G}$ in order. Suppose $T_2(\tilde{e}_1) = c_1, T_2(\tilde{e}_2) = k_1 - c_1$. $T_2(\tilde{e}_i) = c_i, T_2(\tilde{e}_i) = k_1 - c_i$, and so on. Likewise, $\Gamma_1(\tilde{e}_1) = c_1, \Gamma_1(\tilde{e}_2) = k_1 - c_1, \Gamma_1(\tilde{e}_i) = k_1 - c_i$, $\Gamma_2(\tilde{e}_i) = k_1 - c_i$, and so on; $F_1(\tilde{e}_1) = c_1, F_1(\tilde{e}_2) = k_1 - c_1, F_1(\tilde{e}_i) = c_1, F_2(\tilde{e}_i) = k_1 - c_i$, and so on.

Hence, $T_2(\tilde{e}_i) = \begin{cases} c_1, & \text{if } i \text{ is odd,} \\ k_1 - c_1, & \text{if } i \text{ is even.} \end{cases}$

Therefore, $T_2(\tilde{e}_i) = T(\tilde{e}_{2n+1}) = c_1$. Consequently, if $\tilde{e}_1$ and $\tilde{e}_{2n+1}$ connected at a vertex $v_1$, then $d_T(v_1) = k_1, d_T(\tilde{e}_1) + d(\tilde{e}_{2n+1}) = k_1, c_1 + c_1 = k_1, 2c_1 = k_1/2$. \hfill $\Box$

Remark 3. For TCPFG, the above theorem does not hold.

Example 13. The following PFG supports the above remark. In Figure 14, the defined concept is explained.

Theorem 4. Let $G$ be a crisp graph and $\tilde{G}$ be an even cycle. Then, $G$ is CPFG $\Leftrightarrow (T_2, \tilde{f}_2, F_2)$ which is a CF or different edges have same truth membership, abstinence membership, and false membership values.

Proof. Assume $(T_2, \tilde{f}_2, F_2)$ is a CF, then obviously $\tilde{G}$ is a constant PFG. Conversely, suppose that $\tilde{G}$ is $(k_1, k_2, k_3)$CPFG. Consider $\tilde{e}_1, \tilde{e}_2, \tilde{e}_3, \ldots, \tilde{e}_{2n}$ to be the edges of even cycle $G$ in that order. By theorem (3.3),

$$T_2(\tilde{e}_i) = \begin{cases} c_1, & \text{if } i \text{ is odd,} \\ k_1 - c_1, & \text{if } i \text{ is even.} \end{cases}$$

(4)

4.1. Properties of Constant PFG

Theorem 5. If a c CPFG is an odd cycle, then there is no PF bridge and no PF cut vertex.

Proof. Suppose $G$ is a crisp graph having odd cycle and $\tilde{G}$ is a constant PFG. Then, $(T_2, \tilde{f}_2, F_2)$ is a CF. Consequently, deleting any vertex does not decrease the strength of
Suppose \( (T_2, \Gamma_2, F_2) \) is constant function but no totally constant PFG.

\[ \tilde{v}_1(0.4, 0.2, 0.4) \quad (0.4, 0.3, 0.3) \quad \tilde{v}_3(0.3, 0.3, 0.3) \quad \tilde{v}_2(0.2, 0.2, 0.3) \]

\[ \tilde{v}_4(0.3, 0.2, 0.4) \quad (0.3, 0.1, 0.3) \quad \tilde{v}_5(0.3, 0.3, 0.4) \]

Figure 14: \( (T_2, \Gamma_2, F_2) \) is constant function but no totally constant PFG.

\[ \tilde{v}_1(0.3, 0.2, 0.4) \quad (0.3, 0.1, 0.3) \quad \tilde{v}_3(0.5, 0.1, 0.3) \quad \tilde{v}_2(0.4, 0.1, 0.4) \]

\[ \tilde{v}_4(0.3, 0.1, 0.4) \quad (0.3, 0.1, 0.4) \quad \tilde{v}_5(0.4, 0.1, 0.4) \]

Figure 16: \( (T_2, \Gamma_2, F_2) \) is constant but there is no PF bridge and no cut vertex.

\[ (0.4, 0.3, 0.3) \quad (0.4, 0.2, 0.4) \quad (0.2, 0.2, 0.3) \quad (0.3, 0.3, 0.3) \quad (0.2, 0.2, 0.3) \]

\[ (0.2, 0.2, 0.3) \quad (0.2, 0.2, 0.3) \]

Figure 15: \( (T_2, \Gamma_2, F_2) \) is CF, then \( \tilde{G} \) is CPFG, but no TCPFG.

Theorem 6. If a CPFG is an even cycle, then there is no PF bridge and no PF cut vertex.

\[ \tilde{v}_1(0.4, 0.2, 0.4) \quad (0.4, 0.3, 0.3) \quad \tilde{v}_3(0.3, 0.3, 0.3) \quad \tilde{v}_2(0.2, 0.2, 0.3) \]

\[ (0.3, 0.2, 0.4) \quad (0.3, 0.1, 0.3) \quad \tilde{v}_4(0.3, 0.2, 0.4) \quad (0.3, 0.1, 0.3) \]

\[ (0.3, 0.3, 0.4) \quad (0.3, 0.3, 0.4) \]

Proof. Suppose \( G \) is a crisp graph having even cycle and \( \tilde{G} \) is a CPFG. Then, by Theorem 5, \( (T_2, \Gamma_2, F_2) \) is a CF or different edges have same truth membership, abstinence membership, and false membership values.

Case (i). If \( (T_2, \Gamma_2, F_2) \) is CF, then deleting any vertex does not decrease the strength of connectedness between any pair of vertices. Therefore, \( \tilde{G} \) is no bridge and no PF cut vertex.

Case (ii). Straight forward.

Remark 5. For TPFG, the above theorem does not hold.

Example 15. Figure 16 supports the above remark 5 in which the PFG constant is neither bridge nor cut vertex. Figure 16 explains the defined concept.

5. Application

In this section, the application of CPFG in Wi-Fi network system is discussed.

The Wi-Fi technology offers Internet access through a wireless network linked to the Internet to the electronic devices and machines that are in its range. The broadcasting of one or more interconnected access points (hotspots) can extend the range of the connection from a small area of a few rooms to a vast area of many square kilometers. The range of Wi-Fi signals depends on the frequency band, radio power output, and the modulation technique. Although the Wi-Fi connection provides easy access to the Internet, it is also a security risk as compared to the wired connection called Ethernet. For gaining access to Internet connection in a wired network connection, it is necessary to gain physical access to a building that has got the Internet connection or break through an external firewall. On the other hand, in a wireless Wi-Fi connection, the requirement for accessing the Internet is just to get within the range of the Wi-Fi. There are two types of Wi-Fi networks, namely, indoor and outdoor Wi-Fi networks. A compact Wi-Fi hotspot device is called an indoor coin Wi-Fi that intends to facilitate all the indoor owners to access the Internet. These provide Wi-Fi signals ranging at 100 meters (outdoor)/30 meters (indoor). This type of Wi-Fi network is discussed and modeled with the help of CPFG.

Since there are four values to deal with, therefore, the CPFG has been applied to a Wi-Fi network. The first value represents the state of connectedness, the second value describes the fluctuating state of the connection of the device amid the connectedness and disconnectedness states, the third value shows the disconnection, and the last value shows that the device is not in the range. Since the structure of an IFG is limited to just two values, i.e., state of connection and disconnection, therefore, a Wi-Fi system is almost impossible to model through the concept of IFG, whereas the CPFG discusses more than these two situations. Consider an outdoor Wi-Fi system that contains four vertices representing the Wi-Fi devices in such a way that there is a block between every two routers and both routers have been giving signals to the block together, as shown in Figure 17. With the help of CPFG, the devices can give a constant signal to each block.

The four vertices in Figure 17 represent four different routers. The edge between each pair of routers shows the strength of the signals of the routers. Each edge and vertex are in the form of a picture fuzzy number where the first value represents the connectivity. The second one describes the fluctuating state of the device, i.e., the device is in range but fluctuates between the connected and disconnected
states, the third value shows disconnection, and the last value indicates that the device is out of the range. The degree of each vertex is calculated using Definition 4. In this case, the degree of every router is same, which interprets that every router has been giving the same signals. It means that each router is providing the same signal to the block. Thus, the idea of CPFG has been successfully applied to practical problems showing its significance.

Table 1 shows the degree of the vertices in Figure 17.

### 5.1. Advantages of PFG

The advantage of PFGs over existing concept of IFGs is that IFGs cannot be used to model the Wi-Fi network systems as it allows to only deal with just two states, i.e., the state of connectedness and the state of disconnection only. The diverse structure of PFGs enables us to deal with uncertain situations with additional types of states, as presented in the application section. The block together is shown in Figure 18. With the help of IFG, the device can give a constant signal to each block. But that IFGs cannot be used to model the Wi-Fi network system because it only allows to deal with two states, i.e., the state of connectedness and the state of disconnection only.

### 6. Conclusion

This manuscript proposes the ideas of PFG and CPFG. Some fundamental graph theoretic concepts are discussed and illustrated with the help of examples. Moreover, the comparison between PFG and IFG is carried out that shows the significance of the proposed concept. Furthermore, the proposed concept is applied to a practical problem of Wi-Fi network system, and results are discussed. More applications in the different fields can be discussed in the proposed framework, such as in engineering and computer sciences.

### Data Availability

No data were used to support the study.

### Conflicts of Interest

The authors declare no conflicts of interest about the publication of the research article.

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