Improved bounds on $W$-$W'$ mixing with ATLAS resonant $WZ$ production data at the LHC at $\sqrt{s} = 13$ TeV

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New charged vector bosons $W'$ decaying into gauge boson pairs $WZ$ are predicted in many scenarios of new physics, including models with an extended gauge sector (EGM). Due to the large variety of models (other unification groups, models with Supersymmetry, Little Higgs Models, Extra Dimensions) the more general EGM approach is here considered. For what concerns $W'$-production, these models are parametrised by two parameters, the $W'$ mass $M_{W'}$ and the $W$-$W'$ mixing parameter $\xi$. The diboson $WZ$ production allows to place stringent constraints on this mixing angle and the $W'$ mass, which we determine and present for the first time by using data from $pp$ collisions at $\sqrt{s} = 13$ TeV recorded by the ATLAS detector at the CERN LHC, with integrated luminosity of 36.1 fb$^{-1}$. By comparing the experimental limits to the theoretical predictions for the total cross section of $W'$ resonant production and its subsequent decay into $WZ$ pairs, we show that the derived constraints on the mixing angle for the benchmark model are rather small, between $10^{-4}$ and $10^{-3}$, i.e., greatly improved with respect to those derived from the global analysis of electroweak data which yield $\xi \lesssim 10^{-2}$. We combine the limits derived from $WZ$ production data with those obtained from the $W' \rightarrow e\nu$ process in order to significantly extend the exclusion region in the $M_{W'}$-$\xi$ parameter plane and obtain the most stringent exclusion limits to date. We present the combined allowed parameter space for the EGM $W'$ boson after incorporating indirect constraints from low energy electroweak data, direct search constraints from Tevatron and from the LHC Run I with 7 and 8 TeV as well as at Run II with 13 TeV data.
Many extensions to the Standard Model (SM) predict the existence of charged and neutral, heavy gauge bosons that could be discovered at the Large Hadron Collider (LHC). In the simplest models these particles are considered copies of the SM $W$ and $Z$ bosons and are commonly referred to as $W'$ and $Z'$ bosons [1]. The Sequential Standard Model (SSM) [2] posits a $W'_{SSM}$ boson with couplings to fermions that are identical to those of the SM $W$ boson but for which the coupling to $WZ$ is absent. The SSM has been used as a reference point for experimental $W'$ boson searches for decades, the results can be re-interpreted in the context of other models of new physics, and it is useful for comparing the sensitivity of different experiments.

At the LHC, a promising way to search for heavy $W'$ bosons is through their single production as an $s$-channel resonance with their subsequent leptonic decays

$$p + p \rightarrow W' + X \rightarrow \ell \nu + X,$$

where in what follows, $\ell = e, \mu$ unless otherwise stated. The Feynman diagram for the $W'$ boson production and its dilepton decay at the parton level is illustrated in Fig. 1. This process (1) offers the simplest event topology for the discovery of a $W'$ with a large production rate and a clean experimental signature. These channels are among the most promising early discoveries at the LHC [3, 4]. There have also been many theoretical studies of $W'$ boson searches [5–13] at the LHC.

The ATLAS and CMS collaborations set limits on the $W'$ production cross section times branching fraction in the process (1), $\sigma(pp \rightarrow W'X) \times \text{BR}(W' \rightarrow \ell\nu)$, for $M_{W'}$ in the 0.15 TeV – 6 TeV range. The most stringent limits on the mass of a $W'_{SSM}$ boson to date come from the searches in the $W' \rightarrow e\nu$ and $W' \rightarrow \mu\nu$ channels by the ATLAS and CMS collaborations using data taken at $\sqrt{s} = 13$ TeV. The ATLAS and CMS analyses were based on data corresponding to an integrated luminosity of 36.1 fb$^{-1}$ and 35.9 fb$^{-1}$ and set a 95% confidence level (CL) lower limit on the $W'_{SSM}$ mass of 5.2 TeV [3, 4].

An alternative $W'$ search channel is the diboson one

$$p + p \rightarrow W' + X \rightarrow WZ + X.$$

The study of gauge boson pair production offers a powerful test of the spontaneously broken gauge symmetry of the SM and can be used as a probe for new phenomena beyond the SM.

Massive resonances that can decay to gauge boson pairs are predicted by many scenarios of new physics, including extended gauge models (EGM) [2, 14], models of warped extra dimensions [15, 16], technicolour models [17, 18] associated with the existence of technirho and other technimesons, and more generic composite Higgs models [19, 20], etc. Searches for exotic heavy particles that decay into $WZ$ pairs are complementary to searches in the leptonic channels $\ell\nu$ of process (1). Moreover, there are other models in which the $W'$ couplings to SM fermions are suppressed, giving rise to a fermiophobic $W'$ with an enhanced coupling to $W$ and $Z$ bosons [1, 21]. It is therefore important to search for $W'$ bosons also in the $WZ$ final state.

Given the large variety of models which predict new heavy charged gauge bosons, it is a natural approach to use a simplified ansatz for such a search [22]. After a discovery of signatures associated to a new boson, detailed studies can be carried out to distinguish between these models and to determine whether the boson belongs to one of the theoretically motivated models such as an EGM, models of warped extra dimensions, technicolour, composite Higgs models, a Little Higgs model, a Left-Right Symmetric model or a totally different one. Following the traditions of direct searches at hadron colliders, such studies are based on the model first proposed in Ref. [2].

While the SSM has often been referred to as a “Reference Model”, we shall here introduce a terminology that distinguishes them [23, 24]. We shall denote as “Reference Model” (RM) the model obtained by simply introducing
ad hoc new heavy gauge bosons: two charged $W^{\pm}$ vector bosons and one neutral $Z'$ as carbon copies of the SM ones. The fermionic couplings (arising from the covariant-derivative terms) are chosen to be the same as for the ordinary $W$ and $Z$ bosons. The only parameters are the masses of the new vector bosons. In the RM, the coupling constants of the $W'$ boson with SM fermions and the pairs of massive SM gauge bosons are the direct transcription of the corresponding SM couplings, so that $g_{W'WZ} = \cot \theta_W$.

This is in contrast to the case of the SSM, in which the $W'$ coupling to $WZ$ is strongly suppressed, $g_{W'WZ} = 0 \ [23, 24]$. It turns out that in the case of the RM, for $W'$ masses larger than $\sim 0.5$ TeV the total $W'$ width becomes larger than its mass, $\Gamma_{W'} > M_{W'} \ [2]$. Since such a state is not interpreted as a particle anymore, the couplings of $W'$ and $Z'$ to the SM $W$ and $Z$ are suppressed manually in the RM. This leads to a moderate width for the new gauge bosons. Note that this suppression may arise in an EGM in a natural manner: if the new gauge bosons and the SM ones belong to different gauge groups, a vertex such as $W'WZ$ is forbidden. They can only occur after symmetry breaking due to mixing of the gauge eigenstates. Triple gauge boson couplings (such as $W'WZ$) as well as the vector-vector-scalar couplings (like $WWH$) arise from the symmetry breaking and may contribute to the $W'$ decay. The vertices are then suppressed by a factor of the order of $(M_W/M_{W'})^2$. With this assumption, the RM with modified trilinear gauge boson coupling and EGM may have comparable branching ratios and very similar experimental signatures.

Heavy spin-1 resonances are a generic prediction of many EGMs. In particular, the EGM introduces $W'$ and $Z'$ bosons with SM couplings to fermions and with modified $W$-$W'$ mixing-induced coupling of the heavy $W'$ to $WZ$. Here, we concentrate on a study of these mixing effects in the decay of $W'$ to $WZ$.

In an EGM, the trilinear gauge boson coupling is modified by a mixing factor

$$\xi = C \times (M_W/M_{W'})^2, \quad (3)$$

where $C$ is a scaling constant that sets the coupling strength. Note that the EGM can be parametrized either in terms of $(M_{W'}, C)$ or in terms of $(M_{W'}, \xi)$. Specifically, in an EGM the standard-model trilinear gauge boson coupling strength $g_{WWZ} (= \cot \theta_W)$ is replaced by $g_{W'WZ} = \xi \cdot g_{WWZ}$. Following the parametrization of the trilinear gauge boson coupling $W'WZ$ presented in [28] for the analysis and interpretation of the CDF data on $p\bar{p} \to W'\to WZ + X$, expressed in terms of two free parameters $\xi$ and $M_{W'}$, we will set, for the first time, $W'$ limits as functions of the mass $M_{W'}$ and mixing factor $\xi$ by using the ATLAS resonant diboson production data [29] collected at a center of mass energy of $\sqrt{s} = 13$ TeV. The presented analysis in the EGM with two free parameters is more general than the previous ones where the only parameter is the $W'$ mass. Two specific cases will be named: for mixing factor $\xi$ equal to either $\xi = 0$ or $\xi = 1$, corresponding to $W'_{SSM}$ and $W'_{RM}$, respectively. In other words, we adopt the terminology

$$W'_{SSM} \equiv W'_{EGM}(\xi = 0), \quad W'_{RM} \equiv W'_{EGM}(\xi = 1). \quad (4)$$

Previous searches for an EGM $W'$ resonance in the $WZ$ channel have been carried out using $p\bar{p}$ collision data at $\sqrt{s} = 1.96$ TeV at the Tevatron and $pp$ collision data at $\sqrt{s} = 7$ and 8 TeV at the LHC. Early results from the Tevatron [28, 30] derived by the CDF and D0 collaborations have put limits, at the 95% CL, on the mass of a $W'$ boson between 285 and 516 GeV and between 188 and 520 GeV, respectively. The ATLAS and CMS collaborations have also set exclusion bounds on the production and decay of a $W'$ boson, in searches using the $\ell\nu\ell'\ell'$ channel, the ATLAS [31] and CMS [32] collaborations have excluded, at the 95% CL, EGM ($\xi = 1$) $W'$ bosons decaying to $WZ$ for $W'$ masses below 1.52 TeV and 1.55 TeV, respectively. Here $\ell'$ stands for an electron or muon. In addition the ATLAS Collaboration has excluded EGM ($\xi = 1$) $W'$ bosons for masses below 1.59 TeV using the $\ell\ell qq$ channel, and below 1.49 TeV using the $\ell\nu q\bar{q}$ channel. These have also been excluded with masses between 1.3 and 1.5 TeV and below 1.7 TeV by the ATLAS [34] and CMS [35] collaborations, respectively, using the fully hadronic final state. To improve the sensitivity to new diboson resonances in the context of the EGM ($\xi = 1$) in order to set the strongest exclusion bounds on the $W'$ masses, the fully leptonic, semi-leptonic and fully hadronic channels at 8 TeV were combined [24]. The result of this combination was interpreted using the EGM $W'$ model with $\xi = 1$ as a benchmark. The observed lower limit on the $W'$ mass was found to be 1.8 TeV. The various decay channels generally differ in sensitivity in different mass regions. The fully leptonic channel, in spite of a lower branching ratio, is expected to be particularly sensitive to low-mass resonances as it has lower backgrounds.

The strongest lower limit on the $W'$ mass set at 13 TeV is $M_{W'} > 3.2$ TeV [1] in the context of the heavy vector-triplet (HVT) model of “weekly-coupled scenario A” [36]. The HVT generalises a large number of models that predict spin-1 charged ($W'$) and neutral ($Z'$) resonances. Such models can be described in terms of just a few parameters: two coefficients $c_F$ and $c_H$, scaling the couplings to fermions, and to the Higgs and longitudinally polarized SM vector

\footnote{Analogous analysis of the $Z$-$Z'$ mixing proposed in [25] and recently performed on the basis of resonant diboson production data in $p\bar{p} \to Z' \to W^+W^-'+X$ at the ATLAS and CMS can be found in e.g. [26, 27].
\footnote{Such a $W'$, described in terms of two parameters is here referred to as the EGM boson.}
bosons respectively, and the strength $g_\nu$ of the new vector boson interaction. Two benchmark models are considered in the HVT scenario. We are interested in one of them, referred to as HVT model-A, with $g_\nu = 1$ because of its similarity to the EGM ($\mathcal{C} = 1$) W' model, that have comparable branching fractions to fermions and gauge bosons.

Limits were also set on the EGM W' boson coupling strength scaling factor $\mathcal{C}$, as functions of $M_{W'}$, within the EGM framework [28, 30, 32, 37, 38]. It was shown that if the coupling between the W' boson and WZ happens to be stronger (weaker) than that predicted by the EGM with $\mathcal{C} = 1$, the observed and expected limits will be more stringent (relaxed).

The properties of W' bosons are also constrained by measurements of EW processes at low energies, i.e., at energies much below the mass $M_{W'}$. Such bounds on the $W$-$W'$ mixing are mostly due to the change in $W$ properties compared to the SM predictions. These measurements show that the mixing angle $\xi$ between the gauge eigenstates must be smaller than about $10^{-2}$ [1].

In this work, we derive bounds on a possible new charged spin-1 resonance (W') in the EGM framework from the available ATLAS data on WZ pair production [29]. The search was conducted for a new W' resonance decaying into a WZ boson pair, where the W boson decays leptonically ($W \to \ell \nu$ with $\ell = e, \mu$) and the Z boson decays hadronically ($Z \to q\bar{q}$ with $q$ quarks). We present results as constraints on the relevant W-$W'$ mixing angle $\xi$ and on the mass $M_{W'}$, and display the combined allowed parameter space for the benchmark W' boson, showing also indirect constraints from electroweak precision data (EW), direct search constraints from the Tevatron and from the LHC with 7 and 8 TeV as well as with 13 TeV data.

The paper is organized as follows. In Sec. II we summarize the relevant cross section and study the $W' \to WZ$ width in the EGM. Then, in Sec. III we show the resulting constraints on the $M_{W'}$-$\xi$ parameter space obtained from diboson and dilepton processes. In Sec. IV we collect and compare the indirect constraints obtained from electroweak precision data, direct search constraints derived from the diboson process at the Tevatron and at the LHC. Also, we explore the role of the dilepton process in reducing the excluded area in the $W'$ parameter plane, and in Sec. V we conclude.

![FIG. 2. Lowest-order Feynman diagram for the W' boson production and decay to the diboson WZ final state.](image)

**II. W' PRODUCTION AND DECAY AT THE LHC**

At lowest order within the EGM, W' production and decay into WZ in proton-proton collisions occurs through quark-antiquark interactions in the $s$-channel, as illustrated by the Feynman diagram shown in Fig. 2. The cross section of process (2) at the LHC can be observed through resonant pair production of gauge bosons WZ. Using the narrow width approximation (NWA), one can factorize the process (2) into the $q\bar{q}' \rightarrow W' \rightarrow WZ$ production and the W' decay,

$$\sigma(pp \rightarrow W' + X \rightarrow WZ + X) = \sigma(pp \rightarrow W' + X) \times BR(W' \rightarrow WZ).$$

(5)

Here, $\sigma(pp \rightarrow W' \rightarrow WZ + X)$ is the total (theoretical) W' production cross section $\sigma(pp \rightarrow W' + X) \times BR(W' \rightarrow WZ) = \Gamma^{W' \rightarrow WZ} / \Gamma_{W'}$, with $\Gamma_{W'}$ the total width of W'. The cross section $\sigma(pp \rightarrow W' + X)$ for the inclusive W' production $pp \rightarrow W' + X$ is derived from the quark subprocess $q\bar{q}' \rightarrow W'$ which can be written as [39]:

$$\hat{\sigma}(q\bar{q}' \rightarrow W') = \frac{\pi |V_{qq'}|^2}{4} g^2 \delta(s - M^2_{W'}).$$

(6)

3 This may however be considered an effective diagram, in the sense that an underlying theory may generate the $W'WZ$ vertex at loop order.
Here, the weak coupling constant $g = e/\sin \theta_W$, and $V_{qq'}$ is the Cabibbo-Kobayashi-Maskawa (CKM) matrix element connecting quark $q$ and antiquark $\bar{q}'$. The hadronic cross section can be obtained by the summation over all contributing quark-antiquark combinations and integration over the momentum fractions \[ \sigma(p_1p_2 \to W' + X) = \frac{K}{3} \int_0^1 dx_1 \int_0^1 dx_2 \sum_q [f_{q|p_1}(x_1, M_{W'}^2)f_{\bar{q}'|p_2}(x_2, M_{W'}^2)] \hat{\sigma}(qq' \to W'). \tag{7} \]

With $\hat{s}$ the parton subprocess c.m. energy squared, and $s$ the proton-proton c.m. energy squared, it is assumed that $\hat{s} = x_1 x_2 s = M_{W'}^2$ is the appropriate scale of the quark distributions. The coefficient of $1/3$ in front of Eq. (7) is a color factor. Furthermore, $f_{q|p_1}(x_1, M_{W'}^2)$ and $f_{\bar{q}'|p_2}(x_2, M_{W'}^2)$ are quark and antiquark momentum distribution functions for the two protons, with $x_1, x_2$ the parton fractional momenta, related to the rapidity $y$ via $x_{1,2} = (M_{W'}/\sqrt{s}) \exp(\pm y)$. The $K$ factor accounts for higher-order QCD contributions. For the numerical computation, we use the CTEQ-6L1 parton distributions [41] with the factorization and renormalization scales $\mu_F^2 = \mu_R^2 = M_{W'}^2 = \hat{s}$. The obtained constraints presented in the following are numerically not significantly modified when $\mu_{F,R}$ is varied in the range from $\mu_{F,R}/2$ to $2\mu_{F,R}$.

![FIG. 3. Branching fraction BR($W' \to WZ$) (solid) vs $M_{W'}$ in the EGM for non-zero $W$-$W'$ mixing factor $\xi = 10^{-3}$ and $10^{-2}$. For the $W' \to e\nu$ mode (dot-dashed), BR($W' \to e\nu$) for $\xi = 0$ ($W'_{\text{SSM}}$) and $\xi = 0.01$ ($W'_{\text{EGM}}$) are shown. The shaded bands indicate the uncertainty resulting from the inclusion of the $WH$ decay mode, the upper and lower bounds correspond to the assumptions $\Gamma_{W'H} = 0$ and $\Gamma_{W'H} = \Gamma_{W'Z}$, respectively.](image)

In the EGM the $W'$ bosons can decay into the SM fermions, gauge bosons ($WZ$), or a pair of an SM boson and a Higgs boson. In the calculation of the total width $\Gamma_{W'}$ we consider the following channels: $W' \to f\bar{f}$, $WZ$, and $WH$, where $H$ is the SM Higgs boson and $f$ are the SM fermions ($f = \ell, \nu, q$). In this study only left-handed neutrinos are considered while possible right-handed neutrinos are assumed to be kinematically unavailable as final states. Also, throughout the paper we shall ignore the couplings of the $W'$ to beyond-SM particles such as SUSY partners and any exotic fermions in the theory, which may increase the width of the $W'$ and hence lower the branching ratio into a $WZ$ pair. As a result, the total decay width of the $W'$ boson is taken to be

$$\Gamma_{W'} = \sum_f \Gamma_{W'}^{f\bar{f}} + \Gamma_{W'}^{WZ} + \Gamma_{W'}^{WH}. \tag{8}$$

The presence of the two last decay channels, which are often neglected at low and moderate values of $M_{W'}$, is due to $W$-$W'$ mixing which is constrained to be tiny. In particular, for the range of $M_{W'}$ values below $\sim 1.0 - 1.5$ TeV, the
dependence of $Γ_{W'}$ on the values of $ξ$ (within its allowed range) induced by $Γ_{W'Z}^{W}$ and $Γ_{W'H}^{W}$ is unimportant because $\sum f_{j}^f$ dominates over diboson partial widths. Therefore, in this mass range, one can approximate the total width as $Γ_{W'} \approx \sum f_{j}^f$, where the sum runs over SM fermions only.

Due to the assumption that the $W'$ and the $W$ have identical couplings to the SM fermions, the total $W'$ width can be expressed in terms of the $W$ width $Γ_{W}$. For $W'$ masses below $m_t + m_b \approx 180$ GeV the kinematically allowed decay channels are identical for the SM $W$ and the total width reads as $Γ_{W'} = (M_{W'}/M_{W}) Γ_{W}$. For $W'$ masses above 180 GeV the decay $W' \to tb$ opens. Since the phase space is enlarged it results in an increase of the $W'$ width by a factor of 4/3, namely $Γ_{W'} = (4M_{W'}/3M_{W}) Γ_{W}$. For heavy $W'$ with mass much larger than $m_t + m_b$, i.e., $\sim 1.5$-5 TeV, the predicted branching fraction is $BR(W' \to ℓν) = 1/12$ (or about 8.2%) for each of the leptonic channels studied, as illustrated in Fig.3 for the case of vanishing $W-W'$ mixing ($ξ = 0$). Under these assumptions (for decays to massless SM fermions), the total widths scale with the mass as $Γ_{W'} = (g_{f}^{2}/4π)M_{W'}$. Allowing also for final-state QED and QCD corrections, one arrives at $Γ_{W'} \approx 3.5% \times M_{W'}$ (see, e.g. [12]).

For heavier $W'$ bosons, the diboson decay channels, $WZ$ and $WH$, start to play an important role because of their significant contribution to the $W'$ total decay width, $Γ_{W'}$, and to the branching ratio $BR(W' \to WZ)$, we are no longer able to ignore them. To be specific, we take an approach as model-independent as possible, and for numerical illustration show our results in two simple scenarios. In the first scenario, we treat the model as effectively having a suppressed partial width of $W' \to WH$ with respect to that of $W' \to WZ$, i.e., $Γ_{WH}^{W'} \ll Γ_{WZ}^{W'}$, so that one can ignore the former, taking $Γ_{W'} \approx 0$. In this case, numerical results with our treatment will serve as an upper bound on the size of the signal. The second scenario assumes that both partial widths are comparable, $Γ_{WH}^{W'} \approx Γ_{WZ}^{W'}$ for heavy $M_{W'}$ as required by the equivalence theorem [43]. In particular, the equivalence theorem requires that $W'$ decays into fields that are part of the same Higgs doublet (e.g., longitudinal Z and H) have equal decay widths up to electroweak symmetry breaking effects and phase-space factors [9]. While the equivalence theorem might suggest a value for $BR(W' \to WH)$ comparable to $BR(W' \to WZ)$, the $WWH$ coupling is actually quite model dependent [9]. In the numerical analysis presented below, we will consider both scenarios. In the second scenario, $Γ_{W'}$ would be larger, with a suppression of the branching ratio to $WZ$, and the bounds from LHC (and the ability for observing the $W-W'$ mixing effect) would be reduced.

Note also that for all $M_{W'}$ values of interest for LHC the width of the $W'$ boson is considerably smaller than the experimental mass resolution $ΔM$ ($M ≡ \sqrt{s}$) for which we adopt the parametrization in reconstructing the diboson invariant mass of the $WZ$ system, $ΔM/M ≈ 5\%$, as proposed, e.g., in [44, 45]. This condition validates the NWA adopted in this work.

The expression for the partial width of the $W' \to WZ$ decay channel in the EGM can be written as [2]:

$$Γ_{W'}^{WZ} = \frac{α_{em}}{48} \cot^2 θ_{W} M_{W'} \frac{M_{W'}^{4}}{M_{W}^{2} M_{Z}^{2}} \left[ \left( 1 - \frac{M_{Z}^{2} - M_{W'}^{2}}{M_{W'}^{2}} \right)^{2} - 4 \frac{M_{W}^{2}}{M_{W'}^{2}} \right]^{3/2} \times \left[ 1 + 10 \left( \frac{M_{W}^{2} + M_{Z}^{2}}{M_{W'}^{2}} \right) + \frac{M_{W}^{4} + M_{Z}^{4} + 10 M_{W}^{2} M_{Z}^{2}}{M_{W'}^{4}} \right] \cdot ξ^{2}.$$  \hspace{1cm} (9)

As one can see from Eqs. [8] and [9], in the first scenario where $Γ_{W'}^{WH} = 0$, for a fixed mixing factor $ξ$ and at large $M_{W'}$ where $Γ_{W'}^{WZ}$ dominates over $\sum f_{j}^f$, the total width increases rapidly with the $W'$ mass because of the quintic dependence on the $M_{W'}$ mass of the $WZ$ mode, $Γ_{W'}^{WZ} \propto M_{W'} \cdot M_{W}^{4} / (M_{W}^{2} M_{Z}^{2})$, which corresponds to the production of longitudinally polarized $W$ and $Z$ in the decay channel $W' \to W_{L}Z_{L}$. In this case, the $WZ$ mode becomes dominant and $BR(W' \to WZ) \to 1$, while the fermionic decay channels ($\sum f_{j}^f$) are increasingly suppressed. However, in the second scenario with $Γ_{W'}^{WH} = Γ_{W'}^{WZ}$, $BR(W' \to WZ) \to 0.5$ when $M_{W'}$ increases, as is demonstrated in Fig.3 in particular for larger allowed value of the mixing factor, $ξ = 0.01$. Also, Fig.3 shows that the branching ratio of $W'$ to fermions, e.g. $BR(W' \to ℓν)$, decreases as $ξ$ increases. This is opposite to the diboson decay mode of $W' \to WZ$ where the branching ratio increases as $ξ$ increases.

## III. CONSTRAINTS ON $W'$ FROM THE DIBOSON AND DILEPTON PROCESSES

### A. $W-W'$ mixing effects in $W' \to WZ$

Here, we present an analysis, employing the most recent measurements of diboson processes provided by ATLAS [29]. In Fig. [4] we show the observed and expected 95% C.L. upper limits on the production cross section times the branching fraction, $σ_{95\%} \times BR(W' \to WZ)$, as a function of the $W'$ mass, $M_{W'}$. The expected upper limit set on the signal cross section is the greatest value of the signal cross section that is not excluded with 95% confidence. The
data analyzed comprises $pp$ collisions at $\sqrt{s} = 13$ TeV, recorded by the ATLAS (36.1 fb$^{-1}$) detector [29] at the LHC. As mentioned above, ATLAS analyzed the $WZ$ production in the process (2) through the semileptonic final states.

FIG. 4. Observed and expected 95% C.L. upper limits on the production cross section times the branching fraction, $\sigma_{95\%} \times BR(W' \rightarrow WZ)$, as a function of the $W'$ mass, $M_{W'}$, showing ATLAS data for 36.1 fb$^{-1}$ [29]. Theoretical production cross sections $\sigma(pp \rightarrow W') \times BR(W' \rightarrow WZ)$ for the EGM are calculated from PYTHIA 8.2 with a $W'$ boson mass-dependent $K$-factor used to correct for NNLO QCD cross sections, and given by solid curves, for mixing factor $\xi$ ranging from 0.01 and down to 0.0005. The shaded bands are defined like in Fig. 3. The area lying below the long-dashed curve labelled by NWA corresponds to the region where the $W'$ resonance width is predicted to be less than 5% of the resonance mass, in which the narrow-resonance assumption is satisfied. The lower boundary of the region excluded by the unitarity violation arguments is also indicated by the dot-dashed curve.

Then, for $W'$ we compute the LHC theoretical production cross section multiplied by the branching ratio into $WZ$ bosons, $\sigma(pp \rightarrow W') \times BR(W' \rightarrow WZ)$, as a function of the two parameters ($M_{W'}$, $\xi$), and compare it with the limits established by the ATLAS experiment, $\sigma_{95\%} \times BR(W' \rightarrow WZ)$. Our strategy in the present analysis is to adopt the SM backgrounds that have been carefully evaluated by the experimental collaboration and simulate only the $W'$ signal. We set cross section limits on $W'$ as functions of $M_{W'}$ and $\xi$. Our results extend the sensitivity beyond the corresponding CDF Tevatron results [28, 30] as well as the ATLAS and CMS sensitivity attained at 7 and 8 TeV in [28, 30, 32, 37, 38]. Also, for the first time, we set $W'_\text{EGM}$ limits as functions of mass $M_{W'}$ and mixing factor $\xi$ at the LHC from the 13 TeV data with a luminosity of 36.1 fb$^{-1}$.

In Fig. 4, the inner (green) and outer (yellow) bands around the expected limits represent $\pm 1\sigma$ and $\pm 2\sigma$ uncertainties, respectively. The simulation of signals for the EGM $W'$ is based on an adapted version of the leading order (LO) PYTHIA 8.2 event generator [40]. A mass-dependent $K$ factor is used to rescale the LO PYTHIA prediction to the next-to-next-to-leading-order (NNLO) in $\alpha_s$. The theoretical $W'$ production cross section $\sigma(pp \rightarrow W')$ is scaled to a NNLO calculation in $\alpha_s$ by ZWPROD [31, 33, 47], given by solid curves, and shown for mixing factor $\xi$ ranging from 0.01 and down to 0.0005. The factorization and renormalization scales are set to the $W'$ resonance mass.

As was explained in connection with Fig. 3, the upper (lower) boundary of the shaded areas correspond to a scenario where the contribution of the decay channel $W' \rightarrow WH$ to the total $W'$ decay width of Eq. (5) is $\Gamma_{W'}^{WH} = 0$ ($\Gamma_{W'}^{WZ} = \Gamma_{W'}^{WZ}$). The area below the long dashed curve labelled “NWA” corresponds to the region where the $W'$ resonance width is predicted to be less than 5% of its mass, corresponding to the best detector resolution of the searches, where the narrow-resonance assumption is satisfied. In addition, in Fig. 4 we plot a curve labelled “Unitarity limit” that correspond to the unitarity bound (see, e.g. [43] and references therein), where it was shown that the saturation of unitarity in the elastic scattering $W^\pm Z \rightarrow W^\pm Z$ leads to the constraint $g_{W'WZ_{\text{max}}} = g_{W'WZ} \cdot M_{Z}^2 / (\sqrt{3} M_{W'} M_{W})$. 
FIG. 5. Solid (dashed): observed (expected) 95% C.L. upper bound on the $W'$ production cross section times branching ratio to two leptons, $\sigma_{95\%} \times \text{BR}(W' \rightarrow \nu\ell)$, obtained at the LHC with integrated luminosity $L_{\text{int}}=36.1$ fb$^{-1}$ by the ATLAS collaboration [3]. Thin lines: theoretical production cross section $\sigma(pp \rightarrow W') \times \text{BR}(W' \rightarrow \nu\ell)$ for the EGM $W'$ boson, calculated from PYHTHIA 8.2 with an NNLO $K$ factor. These curves in descending order correspond to representative values of the $W$-$W'$ mixing factor $\xi$ from 0 to 0.01. The shaded bands are defined like in Fig. 3.

This bound was obtained under the assumption that the couplings of the $W'$ to quarks and to gauge bosons have the same Lorentz structure as those of the SM, but with a rescaled strength.

The theoretical curves for the cross sections $\sigma(pp \rightarrow W') \times \text{BR}(W' \rightarrow WZ)$, in descending order, correspond to values of the $W$-$W'$ mixing factor $\xi$ from 0.01 to 0.0005. The intersection points of the expected (and measured) upper limits on the production cross section with these theoretical cross sections for various $\xi$ give the corresponding lower bounds on $(M_{W'}, \xi)$, to be displayed below in Sec. IV.

B. $W$-$W'$ mixing effects in $W' \rightarrow \ell\nu$

The above analysis was for the diboson process [2], employing one of the most recent ATLAS measurements [29]. Next, we turn to the dilepton production process (1), this process gives valuable complementary information. Unlike the SSM, where there is no $W$-$W'$ mixing, in the EGM we consider a non-zero mixing $\xi$ in the analysis of the $W' \rightarrow \ell\nu$ process. As described in Sec. II, this results in a modification of $\text{BR}(W' \rightarrow \nu\ell)$.

We compute the $W'$ production cross section at LO with PYTHIA 8.2 [46] at the LHC, $\sigma(pp \rightarrow W')$, multiplied by the branching ratio into two leptons, $\ell\nu$ (here $\ell=e$), i.e., $\sigma(pp \rightarrow W') \times \text{BR}(W' \rightarrow \nu\ell)$, as a function of $M_{W'}$. A mass-dependent $K$ factor is applied, based on NNLO QCD cross sections as calculated with FEWZ 3.1 [49, 50]. The $K$ factor varies approximately from 1.3 to 1.1 for the range of $W'$ masses studied in this analysis, namely from 0.5 to 6.0 TeV. The NNLO corrections decrease with $W'$ boson masses up to around 4.5 TeV [51]. For higher $W'$ masses, the $K$ factor increases again and becomes similar to the low-mass values.

The product of the NNLO $W'$ theoretical production cross section and branching fraction, $\sigma(pp \rightarrow W') \times \text{BR}(W' \rightarrow e\nu)$, for the $W'$ boson for EGM strongly depends on the $W'$ mass, and is for illustrative purposes given by thin solid curves, in descending order correspond to values of the mixing factor $\xi$ from 0.0 to 0.01, as displayed in Fig. 5. Further, we compare the theoretical cross section $\sigma(pp \rightarrow W') \times \text{BR}(W' \rightarrow e\nu)$ with the upper limits of $\sigma_{95\%} \times \text{BR}(W' \rightarrow e\nu)$ established by the ATLAS experiment [3] for 36.1 fb$^{-1}$. Qualitatively, the decrease of the theoretical cross section with increasing values of $\xi$ can be understood as follows: For increasing $\xi$, the $W' \rightarrow WZ$ mode will at high mass $M_{W'}$ become more dominant (as illustrated in Fig. 3), and $\text{BR}(W' \rightarrow e\nu)$ will decrease correspondingly.
Comparison of $\sigma(pp \to W') \times \text{BR}(W' \to e\nu)$ vs $\sigma_{95\%} \times \text{BR}(W' \to e\nu)$ displayed in Fig. 5 allows us to read off an allowed mixing for a given mass value, higher masses are allowed for smaller mixing, for the reason stated above. That comparison can be translated into constraints on the two-dimensional $M_{W'} - \xi$ parameter plane, as will be shown in the next Sec. IV.

The above results are based on data corresponding to an integrated luminosity of 36.1 fb$^{-1}$ taken by the ATLAS collaboration at $\sqrt{s} = 13$ TeV in 2015 and 2016 [3]. However, recently the ATLAS collaboration presented preliminary results on searching for a $W'$ boson conducted in the $W' \to \ell\nu$ channel [1] based on 79.8 fb$^{-1}$ of $pp$ collision data collected in 2015 (3.2 fb$^{-1}$), 2016 (33.0 fb$^{-1}$) and 2017 (43.6 fb$^{-1}$) at a centre-of-mass energy of $\sqrt{s} = 13$ TeV [51]. While the latter analysis followed closely the same procedure as in Ref. [3], the sensitivity of the search presented in [51] was improved due to the inclusion of the 2017 dataset. Specifically, this corresponds to an improvement of approximately $\sim 0.5$ TeV in mass reach compared to the previous ATLAS analysis [3] which did not include the 2017 data and where a lower limit on the $W'_{SSM}$ mass of 5.2 TeV was set at 95% CL. Those preliminary results have not been included in our present analysis.

IV. SUMMARIZING CONSTRAINTS ON THE $W$-$W'$ MIXING

As described above, both the diboson mode and the dilepton process yield limits on the $(M_{W'}, \xi)$ parameter space. These are rather complementary, as shown in Fig. 6, where we collect these and other limits for the considered EGM model. The limits arising from the diboson channel are basically excluding large values of $\xi$, strongest at intermediate masses $M_{W'} \sim 2 - 4$ TeV. The limits arising from the dilepton channel, on the other hand, basically exclude masses $M_{W'} \lesssim 5.2$ TeV, with only a weak dependence on $\xi$. Also, we show the unitarity limits discussed above, as well as the upper bound for the validity of the NWA, indicated as dash-dotted and long-dashed lines, respectively.

Interestingly, Fig. 6, which is dedicated to the EGM model, shows that at high $W'$ masses, the limits on $\xi$ obtained
from the ATLAS diboson resonance production search at 13 TeV and at time-integrated luminosity of 36.1 fb$^{-1}$ are substantially stronger than those derived from the low-energy electroweak data (EW), which are of order $\sim 10^{-2}$

For completeness, we display limits on the $W'$ parameters from the CDF and D0 (Tevatron) as well as from ATLAS and CMS obtained at 7 and 8 TeV of the LHC data taking in Run I. Fig. 6 shows that the experiments CDF and D0 at the Tevatron exclude EGM $W'$ boson with $\xi \gtrsim 2 \cdot 10^{-2}$ and 0.6 TeV $< M_{W'} < 1$ TeV at the 95% C.L., whereas LHC in Run I improves those constraints excluding $W'$ boson parameters at $\xi \gtrsim 2 \cdot 10^{-3}$ in the mass range of 0.6 TeV $< M_{W'} < 2$ TeV. The most stringent exclusion to date in the $M_{W'}$-$\xi$ parameter plane is derived from $WZ$ production data with ATLAS results for time-integrated luminosity of 36.1 fb$^{-1}$ at 13 TeV. Specifically, the EGM $W'$ boson is excluded at $\xi \gtrsim 6 \cdot 10^{-4}$ within the range 0.5 TeV $< M_{W'} < 5.2$ TeV.

Furthermore, we could extrapolate the experimental sensitivity curves for higher expected luminosity downwards by a factor of $1/\sqrt{\mathcal{L}}$, for the $M_{W'}$ mass range which was not statistically limited (i.e., where there are events compatible with the SM background), where $\mathcal{L}$ is the ratio of the full integrated luminosity of 139 fb$^{-1}$ that was collected by the end of Run II $^{[22, 53]}$, to the already analyzed integrated luminosity of 36.1 fb$^{-1}$ in the ATLAS experiment. It is clear that further improvement on the constraining of this mixing can be achieved from the analysis of such data. At fixed $M_{W'}$ the exclusion constraint on $\xi$ scales as $\sim \mathcal{L}_{\mathrm{int}}^{-1/4}$ when statistical errors dominate. The increase of the time-integrated luminosity from 36.1 fb$^{-1}$ to 139 fb$^{-1}$ will allow to set stronger constraints on the mixing angle $\xi$ by a factor of $\approx 1.4$.

We find that the LHC limits obtained at 13 TeV and time-integrated luminosity, $\mathcal{L}_{\mathrm{int}} = 36.1$ fb$^{-1}$, already improves on the EW limits approximatively by one order of magnitude.

Further improvement in placing limits on the $W'$ mass and $W$-$W'$ mixing parameter is feasible in fully-hadronic $WZ \rightarrow qqqq$ final states using the full Run II data set $^{[53]}$. The recent analysis performed in $^{[53]}$ is able to largely improve on the results above for $\sim 36$ fb$^{-1}$ mostly due to the use of novel reconstruction and analysis techniques. Our fast and approximate estimation based on the full (preliminary) Run II data set shows that the improvement in expected upper limits on $\xi$ for the $WZ$ channel at $\sim 3$ TeV is about a factor of two smaller than that presented here.

However, a detailed analysis of the $W$-$W'$ mixing effects in the fully-hadronic $WZ \rightarrow qqqq$ final states is beyond the scope of the present paper and will be presented elsewhere.

V. CONCLUDING REMARKS

Exploration of the diboson $WZ$ production at the LHC with 13 TeV data allows to set stringent constraints on the $W$-$W'$ mixing angle and $W'$ mass, $M_{W'}$. We derived such limits by using data recorded by the ATLAS detector at the CERN LHC, with integrated luminosity of $\sim 36.1$ fb$^{-1}$. By comparing the experimental limits to the theoretical predictions for the total cross section of $W'$ resonant production and its subsequent decay into $WZ$ pairs, we show that the derived constraints on the $W$-$W'$ mixing angle for the EGM model are substantially improved, by a factor of one order of magnitude, with respect to those derived from the global analysis of low energy electroweak data, as well as from the diboson production study performed at the Tevatron and those based on the LHC Run I. Also, the role of the $W'$ dilepton decay channel in reducing the allowed parameter space was adopted. Further constraining of this mixing can be achieved from the analysis of data already collected by the end of Run II, still to be analyzed. The new LHC bound starts to become highly competitive with the constraints coming from low-energy EW studies and after the LHC Run I.

In addition, our work shows that accounting for the contribution of the $W'$ boson decay channel, $W' \rightarrow WH$, to the total width $\Gamma_{W'}$ does not dramatically affect the bounds on the mixing parameter $\xi$ obtained in the scenario of a vanishing $WH$ mode. Namely, it turns out that for the higher $W'$ masses the constraints on $W$-$W'$ mixing are relaxed by a few relative percent for the $WZ$ channel as illustrated in Fig. 6. One should also note that in this paper, for the sake of compactness of the graphic material, we limited ourselves to an analysis of experimental data from the ATLAS detector only. Our further analysis shows that the corresponding CMS data $^{[54, 55]}$ yields bounds on the mixing parameter $\xi$ and the $W'$ boson mass that agree with the results based on the ATLAS data.

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4 The latter ATLAS and CMS constraints depicted in Fig. 6 were obtained from resonant diboson production data collected at low energies, 7 and 8 TeV, by translating limits on the gauge coupling strength $C$ vs $M_{W'}$ $^{[22, 37, 53]}$ onto the $M_{W'}$-$\xi$ parameter plane, see Eq. (3).

5 Such scaling law is also adopted for evaluation of the $Z$-$Z'$ mixing strength vs $\mathcal{L}_{\mathrm{int}}$ in the process $pp \rightarrow Z' + X \rightarrow W^+W^- + X$ $^{[28, 27]}$. 
work of PO has been supported by the Research Council of Norway.

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