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Direct laser cooling to Bose-Einstein condensation in a dipole trap

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We present a method for producing three-dimensional Bose-Einstein condensates using only laser cooling. The phase transition to condensation is crossed with $2.5 \times 10^4$ $^{87}$Rb atoms at a temperature of $T_e = 0.6 \mu$K after 1.4 s of cooling. Atoms are trapped in a crossed optical dipole trap and cooled using Raman cooling with far-off-resonant optical pumping light to reduce atom loss and heating. The achieved temperatures are well below the effective recoil temperature. We find that during the final cooling stage at atomic densities above $10^{15}$ cm$^{-3}$, careful tuning of trap depth and optical-pumping rate is necessary to evade heating and loss mechanisms. The method may enable the fast production of quantum degenerate gases in a variety of systems including fermions.

Quantum degenerate gases provide a flexible platform with applications ranging from quantum simulations of many-body interacting systems [1] to precision measurements [2]. The standard technique for achieving quantum degeneracy is laser cooling followed by evaporative cooling [3] in magnetic [4,5] or optical traps [6]. Evaporation is a powerful tool, but its performance depends strongly on atomic collisional properties and it requires removal of most of the initially trapped atoms. Laser cooling gases to degeneracy could alleviate those issues, but it has proven difficult to implement.

The elusiveness of laser cooling to Bose-Einstein condensation (BEC) [4,5] for more than two decades [8-11] can be understood as follows: optical cooling requires spontaneous photon scattering that moves entropy from the atomic system into the light field. Such scattering sets a natural atomic temperature scale $T_r$ associated with the recoil momentum from a single photon of wavelength $2\pi\lambda$ and an associated atomic thermal de Broglie wavelength $\lambda_{dB} = \sqrt{2\pi\hbar^2/(mk_BT_r)} \sim \lambda$. Here $\hbar$ is the reduced Planck constant, $m$ the atomic mass, and $k_B$ the Boltzmann constant. BEC must then be achieved at relatively high critical atomic density $n_c \sim \lambda_{dB}^{-3} \sim \lambda^{-3}$, where inelastic collisions result in heating and trap loss. In particular, light-induced collisional loss becomes severe when $n \gtrsim \lambda^{-3}$ [12,13].

For strontium atoms, where cooling on a spectrally narrow transition is available, a strongly-inhomogeneous trapping potential has been used to cool a lower-density thermal bath while decoupling the emerging condensate from the cooling light [14]. Very recently, based on similar principles to the ones presented here, an array of small, nearly one-dimensional condensates has been prepared using degenerate Raman sideband cooling [15,16] of $^{87}$Rb atoms in a two-dimensional optical lattice [17].

In this Letter, we demonstrate Raman cooling [14,15–21] of an ensemble of $^{87}$Rb atoms into the quantum degenerate regime, without evaporative cooling. Starting with up to $1 \times 10^6$ atoms in an optical dipole trap, the transition to BEC is reached with up to $2.5 \times 10^4$ atoms within a cooling time of $\sim 1$ s. As discussed in detail below, the essential components of our technique are (i) the use of carefully far-detuned cooling light to reduce atom loss and heating at high atomic densities [12,22,23], (ii) a reduced optical pumping rate during the final stage to avoid heating by photon reabsorption (fustina lente regime [24,26]), (iii) a final cooling of atoms in the high-energy wings of the thermal velocity distribution to achieve sub-recoil cooling, and (iv) careful control of the final trap depth to reduce heating induced by inelastic three-body collisions.

Raman cooling of the optically trapped atoms is a two-
step process where kinetic energy is first removed via a stimulated two-photon Raman transition that simultaneously changes the internal atomic state. Subsequently, entropy is removed in an optical pumping process that restores the original atomic state via the spontaneous scattering of a photon [see Fig. 1(b-c)]. The optical pumping into the state $|5S_{1/2}; F=2, m_F=−2⟩$ along the $z$-axis is performed with $\sigma^−\text{-polarized}$ light. We reduce light-induced loss by using optical pumping light with large negative detuning $\Delta/(2\pi) = −4.33$ GHz from the $|5S_{1/2}; F=2⟩$ to $|5P_{1/2}; F′=2⟩$ transition of the D1-line, choosing a detuning far from molecular resonances [see Fig. 1(b-c) and 27]. The far-detuned $\sigma^−\text{-polarized}$ beam and a $\pi\text{-polarized}$ beam of similar detuning which propagates in the $x−y$ plane [see Fig. 1(a)], drive the stimulated Raman transition to the state $|5S_{1/2}; 2, −1⟩$, simultaneously changing the atomic momentum by the two-photon recoil $\hbar|\Delta k|$ 27. To cool all three directions, we choose $\hbar|\Delta k|$ to have a non-zero projection along any trap eigenaxis.

Cooling is performed in several stages to allow optimization of the cooling as the atomic temperature and density change. Within each stage, the trapping beam powers, optical pumping rate $\Gamma_{sc}$, Raman coupling Rabi frequency $\Omega_R$, and Raman resonance detuning $\delta_R$ are held constant. The first two cooling stages, S1 and S2, are performed in a single-beam optical dipole trap (sODT), after which the atoms are transferred to a crossed optical dipole trap (xODT), where we perform three more cooling stages [X1 to X3, see Fig. 2(a)]. During each stage, we characterize the cooling performance using time-of-flight absorption imaging, extracting the atom number $N$ and temperature $T$. (For the final cooling stage close to the BEC threshold, we exclude the central part of the time-of-flight image from the temperature fit.) We quantify the cooling performance by the classical phase space density $\text{PSD}_c = N(\hbar\omega/(k_BT))^3$, where $\omega = (\omega_x,\omega_y,\omega_z)^{1/3}$ is the geometric mean of the three trapping frequencies. Far from degeneracy, i.e. for a classical gas, $\text{PSD}_c$ equals the true PSD at the center of the cloud, $\text{PSD} = n(0)\lambda_{dB}^3$. The parameters of each stage are optimized to yield the highest $\text{PSD}_c$ at the end of the stage 27.

We load $1\times10^5$ atoms from a magneto-optical trap into the sODT propagating along the $y$-direction with a $10 \mu m$ waist [Fig. 1(a)]. After cooling in stage S1 (see Fig. 2), the trap power and vibration frequencies are reduced, thereby lowering the density and therefore the loss in stage S2. For all stages, we verify that the trap remains sufficiently deep to keep evaporative cooling negligible.

During stages S1 and S2 we perform fast cooling over 500 ms from 30 $\mu K$ down to 1.5 $\mu K$, and up to $\text{PSD}_c$ just below unity. The large loss rate during S1 relative to the other stages [see Fig. 2(c)] occurs because the Raman cooling cycle, and hence light-induced collision rate, is faster. The initial cooling at high temperatures $T\approx 30 \mu K$ and densities $n < 7\times10^{13}$ cm$^{-3}$ is quite efficient, with a logarithmic slope of $\gamma = −d(\ln \text{PSD}_c)/d(\ln N) = 7.2$ [see Fig. 3(a)].

After stage S2, the ensemble is sufficiently cold so that it can be efficiently transferred in the xODT by ramping up the second trapping beam (18 $\mu m$ waist, propagating along $x$), and applying a short initial cooling (stage X1). In a similar fashion to the S1-S2 sequence, we reduce the confinement of the xODT and cool further during X2, after which the ensemble is at the threshold to condensation. No condensate appears in X2 despite $\text{PSD}_c$ reaching the ideal-gas value of 1.2 28, which we attribute to a combination of the finite size effect 29, the interaction shift 30, and small calibration errors. After further reduction of the xODT, we are able to cross the BEC transition during X3, as shown by the appearance
of a condensed fraction in the velocity distribution [see Fig. 3(b)]. The onset of BEC is further confirmed by the anisotropic expansion of the central part of the cloud due to trap confinement anisotropy [see Fig. 3(c)].

In order to achieve BEC, the trap depth during X3 must not be too large. For trap depths much larger than \( \sim k_B \times 20 \mu K \) we observe a strong, density-dependent anomalous heating when the Raman cooling is turned off. (Heating rates of up to 10 \( \mu K/s \) are observed at \( n \approx 2 \times 10^{14} \) cm\(^{-3} \) with a trap depth of \( k_B \times 250 \mu K \).) We surmise that at high atomic densities \( n \gtrsim 10^{14} \) cm\(^{-3} \), recombination products of inelastic three-body collisions undergo grazing collisions with trapped atoms, depositing heat in the cloud \( [27] \). This limit on the maximum trap depth is akin to the necessity to maintain, even in the absence of evaporative cooling, a sufficiently low trap depth by applying a so-called “RF-shield” in magnetic traps which allows highly energetic nonthermal atoms to escape \( [31], [32] \).

The BEC transition is crossed with \( N \approx 2.5 \times 10^4 \) atoms at a critical temperature of \( T_c = 0.61(4) \mu K \). We are able to reach condensate fractions \( N_0/N \) up to 7\%. We also verify that if the Raman cooling is turned off during stage X3, the PSD does not increase, and a condensate does not appear. Furthermore, the condensate can be maintained for \( \sim 1 \) s after creation if the cooling is left on, but if the cooling is turned off, the condensate decays within \( \sim 100 \) ms. This confirms that evaporation is insufficient to create or maintain a condensate in this trap configuration, and that the laser cooling is responsible for inducing the phase transition.

For most laser cooling methods, the requisite spontaneous photon scattering sets a recoil temperature limit. Nonetheless, we achieve sub-recoil temperatures by addressing atoms in the high-energy wings of the thermal distribution. The optical pumping \( |2, -1\rangle \rightarrow |2, -2\rangle \) requires on average the spontaneous scattering of three photons, and therefore imparts \( 6E_r \) of energy, where \( E_r = h^2/(2m\lambda^2) = h \times 3.6 \) kHz is the recoil energy of a 795 nm photon. As a result, only atoms with \( K_{\Delta k}/h \gtrsim 29 \) kHz of kinetic energy along the \( \Delta k \)-direction can be cooled at all \( [27] \). This sets an effective recoil temperature \( T_{r_{\text{eff}}} = 2.8 \mu K \). We achieve cooling below this effective recoil limit down to 0.5 \( \mu K \), i.e. a mean kinetic energy \( \langle K_{\Delta k}\rangle/h = 5.2 \) kHz, by detuning the Raman coupling so that atoms with more than the average kinetic energy are addressed by the cooling light \( [27] \). However, this slows down the cooling for temperatures below \( T_{r_{\text{eff}}} \) (stage S2 onwards), while inelastic collisions add an increased heat load at high densities. In X3 when we cross \( T_c \), we find that under optimized cooling the Raman transition removes 15 kHz of kinetic energy, 30% less than the expected \( 6E_r \) of heating (see SM \( [27] \)). This could indicate that the cooling is aided by bosonic stimulation into the condensate during the photon scattering process, in a similar fashion to Ref. \( [33] \).

The improved performance of our scheme compared to previous Raman cooling results \( [9], [20] \) is primarily due to the flexibility to perform optical pumping to a dark state at large detuning from atomic resonances by operating on the D\(_1\)-line. To identify suitable detunings, we separately characterized light-induced losses over a 16 GHz frequency range to the red of the bare atomic transition, as shown in Fig. 4(a), and further detailed in the SM \( [27] \). Fig. 4(b) displays the final atom number and condensate fraction of the optimized sequence as a function of detuning around the value of \(-4.33 \) GHz chosen for the experiment. We find that a suitable detuning has to be maintained within \( \pm 50 \) MHz to ensure good cooling performance.

Another parameter that needs to be optimized is the photon scattering rate \( \Gamma_{sc} \) for optical pumping into the \( |2, -2\rangle \) dark state. Despite the large detuning, the reabsorption of spontaneously scattered optical pumping photons by other atoms is a resonant two-photon process that can lead to excess heating. However, it was shown theoretically \( [24], [25] \), and confirmed experimen-
FIG. 4. (a) Photoassociation loss spectrum. Survival probability of trapped atoms as a function of the detuning $\Delta$ of the optical pumping beam, when scattering $\sim 100$ photons. In substantial portions of the spectrum, the atomic loss is large, due to photoassociation resonances, whereas the peaks correspond to gaps in the photoassociation spectrum away from resonances. The green arrow indicates the detuning used for the data in Fig. 2 and 3. (b) Performance of the full cooling sequence as a function of optical pumping detuning $\Delta$ near a locally optimal detuning. A condensate fraction $N_0/N$ is visible only when the losses are limited. To keep the Raman resonance detuning $\delta_R$ constant between data points, the magnetic field is adjusted to compensate the change in light shift associated with varying $\Delta$. (c) Temperature and condensate fraction as a function of the scattering rate $\Gamma_{sc}$ in the final cooling stage. Here, the intensity of the $\pi$-polarized beam is adjusted to keep the Raman coupling strength constant between data points, and $\delta_R$ is adjusted to optimize the cooling performance for each data point.

tally [34], that the excess heating can be suppressed at sufficiently low scattering rate $\Gamma_{sc}$, such that the confinement and two-photon Doppler broadening reduce the reabsorption probability. This limit is known as the festina lente regime. The degradation of the performance at larger $\Gamma_{sc}$ in Fig. 4(c) is consistent with increased rescattering, as the calculated reabsorption probability approaches unity [27]. A too small value of $\Gamma_{sc}$, on the other hand, leads to higher temperatures as parasitic heating mechanisms cannot be compensated when the cooling is too slow.

While $^{87}$Rb has relatively favorable collision properties (low two-body inelastic loss rate coefficient, and moderate three-body loss rate coefficient in the upper hyperfine manifold), these properties are not unique, and other atomic species may also be suitable for direct laser cooling to BEC. Since the cooling is not deeply subrecoil, relatively high densities $n \sim \lambda^{-3}$ are required for reaching BEC. Thanks to the fast cooling, the effect of inelastic loss is small enough if a cloud is stable at these densities (typ. lifetime $\gtrsim 1$ s at $10^{14}$ cm$^{-3}$). Inelastic processes can be further reduced in an effectively one-dimensional geometry [17], where fermionization of the bosonic wavefunction reduces collisional processes. The demonstrated technique could also be directly applied to fermionic atoms [9], as well as to laser cooled molecules [35, 36].

In conclusion, we have realized the decades-old goal of BEC purely by laser cooling by creating a single, moderately sized Bose-Einstein condensate in a standard crossed optical dipole trap. Notably, the method is consistent with the general theoretical recipe put forward by Santos et al. [26]. Further work is needed to explore the limits of this new technique in terms of speed, condensate size and final temperature. [We observe that the performance is still density-limited, see Fig. 3(a), and verified that when allowing for moderate final evaporation, nearly pure condensates can be created within a cooling time of 1 s.] It may also be interesting to investigate if this technique can be used to experimentally realize an atom laser, where the condensate is created by bosonic stimulation into the atomic final state during the spontaneous photon scattering [37, 38], rather than through thermalizing elastic collisions.

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