1. Introduction

A reliable land cover classification is the key data for a variety of remote sensing applications, such as natural resources prospecting, environmental management and geospatial planning [1]. The CORINE Land Cover (CLC) implementation over whole territory is a mandatory requirement for all countries of the European Union. In reality, land cover accuracy rarely achieves the commonly recommended 85% target [2].

In remote sensing image classification, useful information is determined by physical fields of landscape. Different classes have different spectral reflectance or self radiance. Multispectral imagery and hyperspectral imagery in particular provide more accurate registration of class spectra, which improves the accuracy of classification [3]. There are well known land cover classification methods. These methods are based on interpretation of multidimensional imagery by class identification features [4].

Modern satellite imagery processing includes different methods for supervised and unsupervised land cover classification. However, known algorithms developed during 1960s – 1980s on the basis of statistical or object-oriented paradigm do not provide the required classification accuracy without additional tweaks [5]. Such algorithms include the maximum likelihood (ML) classifier, k nearest neighbors (kNN) classifier, support vector machine (SVM), object-based image analysis (OBIA) [6].

The basic approach to classification of multispectral imagery is an optical signal in every pixel described as a discrete function $E(\lambda)$, $\lambda = 1, \ldots, m$ in a multidimensional spectral space $\Lambda = \{ \lambda \}$. It is obvious that the average classification accuracy of $m$-dimensional radiometric fields will increase asymptotically with the number of spectral samples $m$ increment [7].

An important problem is the limited a priori knowledge of scene extrapolation to a detailed pixel-level classification. Usually it is performed by assigning a learning sample for each class. The classification theory requires a fundamental discriminability of classes in feature space, i.e., from a mathematical point of view, the probability density distribution should be a separable mixture of probability densities of the classes [8].

Known algorithms used in multispectral imagery classification evaluate some quantitative similarity of the current pixel with each of the defined classes. For classical statistical algorithms it is the class probability or the likelihood ratio, for other ones it is a more or less reasonable similarity measure [9].

Land surface remote imagery contains a significant fundamental stochasticity caused by variations in composition and material of objects observed, by temporal changes in imaging condition and radiation transfer environment and by sensor noises [10]. Therefore, a crisp data analysis for remote imagery classification is not always reasonable under such stochasticity. In some cases, better results can be obtained by fuzzy-logic processing.

This paper is structured as follows. Section 2 describes a fuzzy decision tree model implemented in remote sensing imagery classification. Section 3 presents two ways of processing algorithm for both multispectral (without dimensionality reduction) and hyperspectral imagery classification with the aforementioned model. Section 4 discusses preliminary results obtained from test
processing of actual multi- and hyperspectral satellite imagery. Section 5 presents conclusions drawn from this research.

2. Model

A fuzzy logic approach is quite suitable for multispectral imagery classification. A lot of fuzzy classification algorithms are commonly used in remote sensing, including fuzzy c-means (FCM), fuzzy k nearest neighbors (FNN), semi-supervised fuzzy cluster labeling (SFCL), and object-oriented fuzzy classifier (OOCF) [11]. However, all these algorithms are generalizations of the corresponding crisp statistical algorithms. These algorithms have inherited drawbacks in hyperspectral imagery classification. The major drawbacks include equalization of any quantitative estimations on high-dimensional data and computational instability.

In most cases of hyperspectral data processing, optimal selection of spectral bands is used. This reduces the strong information redundancy of hyperspectral imagery and enhances the overall informativity for the actual remote sensing application [12]. A fuzzy decision tree (FDT) is thus an ideal tool for hyperspectral data classification and simultaneous dimensionality reduction [13]. In terms of FDT, fuzzy data source attributes are spectral bands of a multispectral image, and an image classifying FDT is made using an information-theoretic approach. Up to now a simple unordered FDT is implemented in remote imagery classification. In this case, choice of the next fuzzy attribute depends on results of the previous attributes estimation [14 and 15].

The next spectral band \( B_j \) is selected for each branch of the FDT, providing the maximum amount of information about the target fuzzy classification \( C = \{ C_i \}, i = 1, \ldots, n \), at minimal cost using the already known sequence of previous spectral bands \( B_j, j = 1, \ldots, m \) estimates. The amount of such information \( I(C; B_1, \ldots, B_m) \) is a cumulative mutual information between the resulting fuzzy attribute and the source ones. A number of spectral bands already selected can be used as the cost. The band selection criterion then takes the following form

\[
I(C; B_1, \ldots, B_m) \rightarrow \max.
\]

Cumulative mutual information in (1) is calculated according to the rule [15]:

\[
I(C; B_1, \ldots, B_m) = I(C) + I(B_1, \ldots, B_m) - I(C, B_1, \ldots, B_m).
\]

where \( I(C, B_1, \ldots, B_m) \) is the cumulative joint information of fuzzy attributes which is expressed by the equation

\[
I(B_1, \ldots, B_m) = \log_2 m \times n - \log_2 \prod_{i=1}^{m} \mu(B_i),
\]

where \( \mu(B) \) is the \( k \)-th value of the membership function of fuzzy attribute \( B_k \) \( w \) is the number of possible values in a support set of \( B \) attribute.

For spectral bands attributes of multispectral imagery, the support set is just a gradation range of the registered signal in each band, usually uniform over the entire image. The defined (1) criterion provides a recurrent selection of the spectral band that contains the most information about the target classes. To avoid exhaustive search of all spectral bands, growth of the tree should be limited by pruning low-information branches.

3. Algorithm

Practical implementation of the proposed model in classification of remote sensing images should be performed in two ways. For a small number of spectral bands (multispectral image case), all of them are quite informative. For a sufficiently large number of spectral bands (hyperspectral image case) a fully-featured decision tree is built with branch pruning. A decision tree node is transformed into a leaf node, if the relative frequency of any solution alternative solution exceeds some a priori specified level \( \beta \):

\[
2^{-I(C | B_{1}, \ldots, B_{m})} \geq \beta, \quad (4)
\]

where \( I(C | B_{1}, \ldots, B_{m}) \) is cumulative conditional information of decision \( C \) with known values of fuzzy attributes \( B_{1}, \ldots, B_{m} \). This variable can be calculated as

\[
I(C | B_{1}, \ldots, B_{m}) = I(C, B_{1}, \ldots, B_{m}) - I(C), \quad (5)
\]

where \( I(C, B_{1}, \ldots, B_{m}) \) determined by the (3) and

\[
I(C) = \log_2 m \times n - \log_2 \sum_{i=1}^{n} \mu(C_i).
\]

An important stage of algorithm is to bring the source multispectral crisp data into fuzzy form required for FDT operations. In remote sensing, Gaussian distribution functions are usually used for this purpose [16], but in our research histogram-based membership functions in spectral bands were formed. The distributions obtained are smoothed by sliding Gaussian window. As to pixel fuzzification, it was carried out within the Gaussian-weighting two-dimensional window. This incorporates some positive properties of OBIA into the image classification result [17].

The computation takes into account the distribution of possible states of input fuzzy attributes with different membership degrees. A certain weighting factor, which is associated with tree branches up to the current leaf node, was assigned to each spectral band. Similarly, the output image classification contains the membership function values also for all allowable classes. To obtain a crisp (hard) classification, the class with the maximum value of the output membership function must be selected.
4. Results and discussion

The developed algorithm for remote sensing imagery classification using FDT was applied to test land cover classification on real satellite images. All data processing procedures have been coded and debugged with a Free Pascal compiler. All the source DN-data bands of satellite images calibrated through values of radiance at sensor are converted into land surface spectral reflectance to avoid the influence of solar irradiance and atmosphere.

The first type of processing (ranking bands only) was applied to the Sich-2/MSU multispectral 3-bands satellite image fragment (Crimea, Ukraine, November 8, 2011, see Fig. 1a). Supervised classification was performed using FDT. Also a conventional crisp classification using the ML method was carried out as reference. The outputs are shown in Fig. 1b and 1c.

A full-featured processing (a limited FDT with branch pruning) was done over the EO-1/Hyperion hyperspectral 220-bands satellite image fragment (Kiev suburb, Ukraine, March 17, 2012, see Fig. 3a). In the source full-band hyperspectral image, 78 of 220 spectral bands with a better signal-to-noise ratio were preselected for further analysis. A fuzzy decision tree was formed in the first stage of the algorithm, as shown in Fig. 2.

In Fig. 2, decision nodes with codes of evaluating spectral bands are presented as rectangles, and leaf nodes with class numbers are presented as ovals. It is clear that another decision tree will be induced for another hyperspectral image (HSI) or for other classes composition.

The result of the FDT supervised classification is given in Fig. 3c. A spectral angle mapper (SAM) classification was used as a reference (see Fig. 3b) because the generic ML classifier is inoperable over high-dimensional data due to covariance matrices singularization.

Analysis of the classification results leads us to conclude that the FDT algorithm provides a better classification in general. In the Sich-2/MSU multispectral image, arable lands are classified more accurately, sand and concrete are discriminated better, but water surface is identified with less confidence. Even if ground-based validation of test images is not carried out, visual assessment using high-resolution imagery can roughly estimate classification accuracy of 75% for the ML algorithm and 80% for the FDT one. In SAM-based classification of the EO-1/Hyperion hyperspectral test image, a substantial percentage of the land cover was incorrectly classified as water. Correct classification was not observed in the vicinity of high spectral reflectance areas (snow). Artificial cover was falsely detected among deep woodlands, etc. A classification accuracy was estimated as 65% for the SAM algorithm and as 75% for the FDT algorithm. In
The results obtained are supported preliminary by experiments in test processing and analysis of actual multi- and hyperspectral satellite imagery. The problem of achieving the required performance of the developed algorithms and demonstration software modules has not been solved yet. This can be seen in problems with difficult processing of large-size imagery. Moreover, positive results obtained previously must be validated through in situ observations. We look forward to continue our joint research in improving models for FDT-based remote sensing image classification, in particular by implementation of more sophisticated decision strategies and new remote sensing application-oriented informativity metrics entering into the algorithms.

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5. Conclusions

A new algorithm for remote sensing multi- and hyperspectral imagery classification based on a fuzzy decision tree approach has been developed. In some cases, this algorithm provides more exact classification accuracy than traditional ones, approximately by 5-10%. In addition, a significant reduction of data dimensionality (more than 3.5-fold) for hyperspectral imagery processing is ensured by informative spectral bands selection using branch pruning of the decision tree. A proper and productive reduction in data dimensionality is very important for large-scale high-performance practical analysis of remote sensing hyperspectral imagery. The results obtained are supported preliminary by experiments in test processing and analysis of actual multi- and hyperspectral satellite imagery.

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References

[1] Multispectral Remote Sensing in Nature Management (in Ukrainian). LYALKO V.I., POPOV M. O. (Eds). Naukova Dumka, 2006.
[2] BRODSKY, L., BUSHUEV, E., VOLOSHIN, V., KOZLOVA, A., PARSHINA, O., POPOV, M., SABLINA, V., SAKHATSKY, A., SIROTENKO, A., SOUKUP, T., STANKEVICH, S., TARARIKO, A.: The INTAS Project for the Elaboration of Automated Technology of Land Cover Classification: The Scientific Problems, Main Results and Prospects (in Russian). Space Science and Technology, 2009, 15(2):36-48.
[3] LU, D., WENG, Q.: A survey of Image Classification Methods and Techniques for Improving Classification Performance. Intern. J. of Remote Sensing, 2007, 28(5):823-870.
[4] DUDA, T., CANTY, M.: Unsupervised Classification of Satellite Imagery: Choosing a Good Algorithm. Intern. J. of Remote Sensing, 2002, 23(11):2193-2212.

[5] POPOV, M.A., STANKEVICH, S. A., SAKHATSKY, A. I., KOZLOVA, A. A.: Multispectral Imagery Normalized Band-difference Indexes for Land Cover Classification. Proc. of Digital Earth Summit on Geoinformatics (DE’08): Tools for Global Change Research, Potsdam, 2008:333-338.

[6] TSO, B., MATHER, P. M.: Classification Methods for Remotely Sensed Data. Taylor & Francis, 2004.

[7] HO, T. K., BAIRD, H. S.: Large-scale Simulation Studies in Image Pattern Recognition. IEEE Transactions on Pattern Analysis and Machine Intelligence, 1997, 19(10):1067-1079.

[8] FUKUNAGA, K.: Introduction to Statistical Pattern Recognition. Academic Press, 1990.

[9] CHA, S.-H.: Comprehensive Survey on Distance/similarity Measures between Probability Density Functions. Intern. J. of Mathematical Models and Methods in Applied Sciences, 2007, 1(4):300-307.

[10] WOODCOCK, C. E.: Uncertainty in Remote Sensing, in Uncertainty Remote Sensing and GIS. FOODY G.M., ATKINSON P.M. (Eds). John Wiley, 2006:19-24.

[11] CHEN, W., JI, M.: Comparative Analysis of Fuzzy Approaches to Remote Sensing Image Classification. Proc. of 7th Intern. Conference on Fuzzy Systems and Knowledge Discovery (FSKD’10), Yantai, 2010:537-541.

[12] STANKEVICH, S. A.: Quantitative Estimation of Hyperspectral Imagery Informativity for the Remote Sensing Applications (in Ukrainian). Proc. of NAS of Ukraine, 2006, 10:53-58.

[13] LEVASHENKO, V., ZAITSEVA, E., PUURONEN, S.: Fuzzy Classifier Based on Fuzzy Decision Tree. Proc. of the IEEE Intern. Conference Computer as a Tool (Eurocon’07), Warsaw, 2007:823-827.

[14] LEVASHENKO, V., ZAITSEVA, E.: Fuzzy Decision Trees in Medical Decision Making Support System. Proc. of the IEEE Federated Conference on Computer Science and Information Systems (FedCSIS), Szczecin, 2012, 213-219.

[15] STANKEVICH, S., LEVASHENKO, V., ZAITSEVA, E.: Fuzzy Decision Tree Model Adaptation to Multi- and Hyperspectral Imagery Supervised Classification. Proc. of the IEEE Intern. Conference on Digital Technologies, Zilina, 2013, 198-202.

[16] NEDELJKOVIC, I.: Image Classification Based on Fuzzy Logic. The Intern. Archives of the Photogrammetry, Remote Sensing and Spatial Information Sciences, 2004, 34(XXX):83-88.

[17] GOMEZ, D., MONTERO, J.: Fuzzy Sets in Remote Sensing Classification. Soft Computing, 2008, 12(3):243-249.