A Successful 3D Core-Collapse Supernova Explosion Model

David Vartanyan1*, Adam Burrows1, David Radice1,2, M. Aaron Skinner3, Joshua Dolence4
1 Department of Astrophysical Sciences, Princeton University, Princeton, NJ 08544
2 Institute for Advanced Study, 1 Einstein Dr, Princeton NJ 08540
3 Lawrence Livermore National Laboratory, P.O. Box 808, Livermore, CA 94551-0808
4 CCS-2, Los Alamos National Laboratory, P.O. Box 1663 Los Alamos, NM 87545

17 September 2018

ABSTRACT

In this paper, we present the results of our three-dimensional, multi-group, multi-neutrino-species radiation/hydrodynamic simulation using the state-of-the-art code Fornax of the terminal dynamics of the core of a non-rotating 16-M⊙ stellar progenitor. The calculation incorporates redistribution by inelastic scattering, a correction for the effect of many-body interactions on the neutrino-nucleon scattering rates, approximate general relativity (including the effects of gravitational redshifts), velocity-dependent frequency advection, and an implementation of initial perturbations in the progenitor core. The model explodes within ~100 milliseconds of bounce (near when the silicon-oxygen interface is accreted through the temporarily-stalled shock) and by the end of the simulation (here, ~677 milliseconds after bounce) is accumulating explosion energy at a rate of ~2.5×1050 erg s⁻¹. The supernova explodes with an asymmetrical multi-plume structure, with one hemisphere predominating. The gravitational mass of the residual proto-neutron star at ~677 milliseconds is ~1.42 M⊙. Even at the end of the simulation, explosion in most of the solid angle is accompanied by some accretion in an annular region at the wasp-like waist of the debris field. The ejecta electron fraction (Ye) is distributed between ~0.48 and ~0.56, with most of the ejecta mass proton-rich. This may have implications for supernova nucleosynthesis, and could have a bearing on the p- and νp-processes and on the site of the first peak of the r-process. The ejecta spatial distributions of both Ye and mass density are predominantly in wide-angle plumes and large-scale structures, but are nevertheless quite patchy.

Key words: stars - supernovae - general

1 INTRODUCTION

The neutrino mechanism of core-collapse supernovae (CC-SNe) was proposed more than fifty years ago (Colgate & White 1966), but due to the complexity and exotic character of the environment in which it occurs and the realization that hydrodynamic instabilities and turbulence are crucial to explosion in all but a small subset of progenitor stars, credible confirmation of this mechanism and its observational validation have been frustratingly slow. Along with the requirement to incorporate nuclear and particle physics that does justice to the wide range of relevant neutrino-matter interactions and to the equation of state of dense nuclear matter, the centrality of turbulent convective and shock instabilities that break spherical symmetry has necessitated performing theoretical simulations in multiple spatial dimensions. The two-dimensional (2D) simulations (axisymmetric) of the 1990’s lacked detailed neutrino physics, but demonstrated the relevance of neutrino-driven convection (Herant et al. 1994; Burrows et al. 1995). The early years of this millennium introduced another instability (the standing-accretion shock instability, Blondin et al. 2003) and subsequent work built on previous 2D efforts by incorporating general relativity (GR, at various levels of approximation), improving the physical fidelity of the neutrino interactions embedded into the codes, enhancing the spatial resolution of the calculations, and carrying simulations out to later physical times. Summaries of some of this history can be found in reviews by Janka (2012),
Burrows (2013), Müller (2016), and Janka et al. (2016). In fact, progress in understanding the CCSN mechanism has paralleled progress in both physics and computational capability, and such progress has spanned decades. It is only recently that fully three-dimensional (3D) simulations with multi-group neutrino transfer that address all the physical terms and effects, employ state-of-the-art nuclear equations-of-state, and calculate for a physically significant duration have emerged. Though there is still much work to do, the recent advent of codes that address the full dimensional and physics requirements of the CCSN problem represents a watershed in the theoretical exploration of the supernova mechanism. In this paper, we present one such modern simulation of the explosion in 3D of a 16-M⊙ star, using our new supernova code FORNAX (Skinner et al. 2016; Radice et al. 2017; Vartanyan et al. 2018; Burrows et al. 2018; Skinner et al. 2018).

State-of-the-art calculations in 3D exploring the mechanism of CCSN explosions have undergone significant evolution and improvement over the years. Sixteen years ago, Fryer & Warren (2002, 2004) used a smooth-particle hydrodynamics code SNPSH to explore the differences between 2D and 3D simulations and the possible role of rapid rotation. They found their 2D and 3D simulations were similar and that rapid rotation modified the driving core neutrino emissions. However, these simulations employed gray radiation, and did not include inelastic energy redistribution nor velocity dependent transport effects, and ignored GR effects. Parameterized studies in 3D (Nordhaus et al. 2010; Dolence et al. 2013; Hanke et al. 2012; Couch & O’Connor 2014; Couch & Ott 2015) disagreed on the relative difficulty of explosion in 3D vs. 2D. However, these simulations, while boasting improved hydrodynamics algorithms and resolution, used “lightbulb” neutrino driving and did not employ competitive neutrino transfer and microphysics. Using ZEUS-MP on a low-resolution 3D grid, Takiwaki et al. (2012) witnessed the explosion of a 11.2-M⊙ progenitor (Woosley et al. 2002). However, these authors used the sub-optimal IDSA scheme neutrino transfer approach (Liebendörfer et al. 2009), which ignores velocity-dependence, GR, and inelasticity, stitches together the opaque and transparent realms in an ad hoc fashion, uses the problematic “ray-by-ray” approach to multi-D transport, and either neglects “heavy” neutrinos or incorporates them in a “leakage” format. The ray-by-ray approach used by many early and current studies performs multiple one-dimension transport calculations, in lieu of truly multi-D transport, and thereby ignores the important effects of lateral transport (Skinner et al. 2016).

Using the CHIMERA code, Lentz et al. (2015) witnessed the explosion of a 15-M⊙ progenitor star (Woosley & Heger 2007) ~300 milliseconds (ms) after bounce, ~100 ms later than their 2D simulation. These authors used state-of-the-art microphysics and approximate GR, but used multi-group flux-limited diffusion and the reduced-dimension ray-by-ray approach and evolved the inner 6-8 kilometers (km) in spherical symmetry. In addition, they employed the LS220 equation of state (EOS) (Lattimer & Swesty 1991), now known to be inconsistent with known nuclear systematics.

Early low-resolution 3D simulations using the Prometheus-Vertex code (Hanke et al. 2013; Tamborra et al. 2014) found that the 11.2-, 27- (Woosley et al. 2002), and 25-M⊙ (Woosley & Heger 2007) non-rotating progenitors did not explode in 3D, while their 2D counterparts did. Prometheus-Vertex uses state-of-the-art neutrino microphysics, a multi-group variable Eddington factor transport algorithm with approximate GR (Marek et al. 2006), but uses the ray-by-ray+ approximation to neutrino transport. Later, this group (Melson et al. 2015a) witnessed the explosion of a zero-metallicity 9.6-M⊙ progenitor in 3D, a model that explodes easily in 1D (Radice et al. 2017). By making a large strangeness correction to the axial-vector coupling constant in Prometheus-Vertex, Melson et al. (2015b) were able to generate an explosion in 3D of the non-rotating 20-M⊙ progenitor that did not otherwise explode. However, such a large correction may be inconsistent with nuclear experiment (Ahmed et al. 2012; Green et al. 2017). Recently, this group (Summa et al. 2018) has found that rapidly rotating progenitor models (Heger et al. 2005) explode shortly after the accretion of the silicon-oxygen (Si-O) interface. They argue, as do Takiwaki et al. (2016), that a strong non-axisymmetric spiral mode facilitates explosion in the rapidly-rotating context. However, with their default neutrino physics, this group has yet to witness the explosion in 3D of any non-rotating models using Prometheus-Vertex. Moreover, their 3D models were all calculated using the LS220 EOS.

Using the Coconut-FMT code in 3D, Müller (2015) witnessed the explosion of the 11.2-M⊙ progenitor of Woosley et al. (2002) in 3D employing the LS220 nuclear EOS. However, Coconut-FMT employs simplified multi-group neutrino transport, the ray-by-ray approximation, neglects both velocity dependence in the neutrino sector and inelastic scattering, and cuts out the proto-neutron star (PNS) core. Its virtue is that it incorporates conformally-flat GR. Using Coconut-FMT and a 3D 18-M⊙ initial progenitor to provide perturbations, Müller et al. (2017) witnessed what they interpret as a perturbation-aided explosion and the simulation was carried out to an impressive ~2.5 seconds after bounce.

It is only recently that codes with truly multi-dimensional, multi-group transport, without the ray-by-ray compromise and with state-of-the-art microphysics and approximate or accurate GR, have been constructed and fielded. Roberts et al. (2016) used the adaptive-mesh-refinement (AMR) Cartesian code Zelmani with full GR, the M1 moment closure approach, the SFHo nuclear EOS (Steiner et al. 2013), but without velocity dependence in the transport sector or inelastic scattering, to evolve the 27-M⊙ progenitor of Woosley et al. (2002). Using the same code, Ott et al. (2018) explored the 12-, 15-, 20-, 27-, and 40-M⊙ progenitor models of Woosley & Heger (2007). This team witnessed the low-energy explosion of all models, save the 12-M⊙ model. More recently, Kuroda et al. (2016a) have developed a multi-group radiation-hydrodynamic CCSN code with M1 closure, detailed microphysics, and full GR. However, their recent CCSN simulations (Kuroda et al. 2016b) of 11.2-, 40- (Woosley et al. 2002), and 15-M⊙ (Woosley & Weaver 1995) progenitors were done with gray transport and none of their models exploded. A related code using the FLASH architecture, AMR, state-of-the-art microphysics, approximate GR, and M1 transport more recently witnessed no explosion for a 20-M⊙ progenitor, but noted large asymmetries in the Si and O shells that might dynamically aid explosion (O’Connor & Couch 2018).

In this paper, we present the first results in a series of...
3D simulations that employ our new code FORNAX (Skinner et al. 2018). FORNAX is a multi-group, velocity-dependent neutrino transport code that employs the M1 two-moment closure scheme. It incorporates state-of-the-art neutrino microphysics, approximate GR (with gravitational redshifts), inelastic energy redistribution via scattering, and does not employ the ray-by-ray simplification. Furthermore, it uses a dendritic grid that deresolves in angle upon approach to the core, while maintaining good zone sizes. This allows us to include the stellar center while employing a spherical grid but without incurring an onerous Courant time step penalty. We find that the 16-M\(_{\odot}\) progenitor (Woosley & Heger 2007) explodes in 3D, and does so shortly before its 2D counterpart.

Throughout this paper, we explore the dimensional dependence (2D vs. 3D) of the explosion properties. We organize the paper as follows: In §2, we outline the setup of our simulation. We explore the basic explosion properties in the beginning of §3 and the shock evolution in §3.1. In §3.2 and 3.3, we explore the explosion energetics and heating rates and the luminosities and mean energies, respectively. We look at the ejecta composition in §3.4, and study PNS convection in §3.5. We comment in §3.6 on the possibility of the lepton-number emission self-sustained asymmetry (LESA; Tamborra et al. 2014) in our 3D simulation and the lack of the standing accretion-shock instability (SASI). In §4, we conclude with summary comments and observations.

## 2 Numerical Setup and Methods

The progenitor upon which we focus in this paper is the 16-M\(_{\odot}\) model of Woosley & Heger (2007) (which was studied in 2D in Vartanyan et al. 2018), and we employ the state-of-the-art multi-D, multi-group radiation/hydrodynamic code FORNAX (Skinner et al. 2018). Earlier supernova work using FORNAX includes Wallace et al. 2016 (neutrino breakout burst detection), Skinner et al. 2016 (shortcomings of the ray-by-ray approximation in core-collapse simulations), Radice et al. 2017 (low-mass CCSNe), Burrows et al. 2018 (the role of microphysics in CCSNe), Morozova et al. 2018 (gravitational wave signatures of CCSNe), Vartanyan et al. 2018 (CCSNe from 12-25 M\(_{\odot}\)), and Seadrow et al. 2018 (neutrino detection of CCSNe).

FORNAX is a multi-dimensional, multi-group radiation hydrodynamics code originally constructed to study core-collapse supernovae and its structure, capabilities, and variety of code tests are described in Skinner et al. (2018).

The generalization of the equations to approximate general-relativistic gravity and redshifts is described in Appendix A. In 2D and 3D, FORNAX employs a dendritic grid which deresolves at small radii and in 3D along the \(\phi\) axis to avoid overly-restrictive CFL time step limitations, while at the same time preserving cell size and aspect ratios. Our method of deresolving near the polar axis for 3D simulations allows us to partially overcome axial artifacts seen conventionally in 3D simulations in spherical coordinates (see, e.g. Lentz et al. 2015; Müller et al. 2017). FORNAX solves the comoving-frame velocity-dependent transport equations to order \(O(\nu/c)\). The hydrodynamics uses a directionally-unsplit Godunov-type finite-volume scheme and computes fluxes at cell interfaces using an HLLC Riemann solver. For the 3D simulation highlighted in this paper, we employ a spherical grid in \(r, \theta,\) and \(\phi\) of resolution 608\times128\times256. For the comparison 2D simulation, the axisymmetric grid has resolution 608\times128. The radial grid extends out to 10,000 kilometers (km) and is spaced evenly with \(\Delta r \sim 0.5\) km for \(r \lesssim 50\) km and logarithmically for \(r \gtrsim 50\) km, with a smooth transition in between. The angular grid resolution varies smoothly from \(\Delta \theta \sim 1.9^\circ\) at the poles to \(\Delta \theta \sim 1.3^\circ\) at the equator, and has \(\Delta \phi \sim 1.4^\circ\) uniformly. For this project, we used a monopole approximation for relativistic gravity following Marek et al. (2006), as described in Appendix A, and employed the SFHo equation of state (Steiner et al. 2013), which is consistent with all currently known nuclear constraints (Tews et al. 2017).

We solve for radiation transfer using the M1 closure scheme for the second and third moments of the radiation fields (Vaytet et al. 2011) and follow three species of neutrinos: electron-type (\(\nu_e\)), anti-electron-type (\(\bar{\nu}_e\)), and “\(\gamma_{\nu}\”\)-type (\(\nu_{\mu}, \bar{\nu}_\mu, \nu_{\tau}, \bar{\nu}_{\tau}\) neutrino species collectively). We use 12 energy groups spaced logarithmically between 1 and 100 MeV for the electron neutrinos and to 100 MeV for the anti-electron- and “\(\gamma_{\nu}\”\)-neutrinos. The neutrino-matter interactions implemented and the handling of inelastic scattering and energy redistribution of neutrinos off electrons and nucleons are both summarized in Appendix B.

For this paper, we initially evolve collapse in 1D until 10 ms after bounce, and then map to higher dimensions. After mapping, we impose velocity perturbations (for the 2D and 3D, but not 1D, simulations) following Müller & Janka (2015) in three spatially distinct regions (50 – 85 km, 90 – 250 km, and 260 – 500 km), with a maximum speed of 500 km s\(^{-1}\) and harmonic quantum numbers of \(l = 2, m = 1,\) and \(n = 5\) (radial), as defined in Müller & Janka (2015). These perturbations were motivated by Müller et al. (2016), who evolve the last minutes of a 3D progenitor and find convective velocities of almost 1000 km s\(^{-1}\) at the onset of collapse (with a corresponding Mach number of 0.1) in the O-shell around 5000 km with a prominent \(l = 2\) mode.

Our 3D simulation was evolved to 677 ms after core bounce, and required a total resource burn of \(\sim\)18 million CPU-hours on the NERSC/Cori II machine using 16256 cores in parallel.\(^*\)

We note that the 16-M\(_{\odot}\) progenitor was studied in Vartanyan et al. (2018), but with a different setup. In that paper, we did not include initial velocity perturbations, had 20 (instead of 12) energy bins per neutrino species, and employed an angular resolution of 256 polar cells (instead of 128). We also did not map from 1D to 2D 10 ms after bounce, but evolved entirely in 2D. Our grid then extended to 20,000 km (not 10,000 km). For the 2D comparison model in this paper, we maintain these differences to mimic the setup we use for our concurrent 3D run. However, we obtain the same overall results for the 16-M\(_{\odot}\) progenitor seen in Vartanyan et al. (2018).

\(^*\) For comparison, some earlier 3D simulations (e.g., Summa et al. 2018 for a model with slightly lower resolution, but with rotation) required \(\sim\)50–100 million CPU-hours to evolve to 0.5 seconds after bounce.
3 EXPLOSION PROPERTIES

We find that the 16-M$_\odot$ progenitor of Woosley & Heger (2007) explodes in both the corresponding 2D and 3D simulations, at \( \sim 100 \) and \( \sim 120 \) ms after bounce, respectively. The corresponding 1D simulation does not explode. The explosions in 2D and 3D are abetted by the inclusion of detailed microphysics – in particular, inelastic scattering off electrons, nucleons, and the associated energy redistribution, and the decrease in the neutral-current neutrino-nucleon scattering rates due to the many-body effect (Burrows et al. 2018; Horowitz et al. 2017) – as well as a steep density gradient at the silicon-oxygen interface located deep within the progenitor, near an interior mass of \( \sim 1.5\text{-}M_\odot \) (Vartanyan et al. 2018; Ott et al. 2018). Unlike in many recent 3D simulations, we use the SFHo equation of state in this work.

At the end of our 3D simulation, \( \sim 677 \) ms after bounce, the maximum shock radius has reached \( \sim 5000 \) km, with an asymptotic velocity of \( \sim 10,000 \text{ km s}^{-1} \). The diagnostic explosion energy is \( \sim 1.7 \times 10^{50} \) erg by this time. The mass of the core ejecta, defined as neutrino-processed gravitationally unbound material, is \( \sim 0.08 \text{-} M_\odot \) and growing. The corresponding gravitational PNS mass is \( \sim 1.42 \text{-} M_\odot \) and the mean PNS radius \( \sim 29 \) km. These features are explored in greater detail in the later sections and compared to the results in 2D. In all regards, we find that integrated 3D metrics are significantly less variable with time than their 2D analogs.

In Fig. 1, we show a time sequence of the entropy of the 3D simulation, illustrating the highly non-axisymmetric nature of the explosion. By \( \sim 100 \) ms after bounce, shock expansion and explosion are underway, with the outflow initially constituting bubbles interior to the shock. The explosion assumes a bi-cameral structure, with the two hemispheres separated by a plane oriented with \( \theta \sim 40^\circ \) and \( \phi \sim 50^\circ \) in spherical coordinates. Unlike in 2D, the explosion does not orient around any coordinate axis and there is no axial sloshing; any explosion axis that emerges does so naturally and is not imposed. Indeed, the explosion is not isotropic, but has a preferred direction, clockwise-orthogonal to the dividing plane. The left hemispher (in this projection) dominates and we see some fingers along the axis at \( \sim 443 \) ms (3rd panel), but these are accreted soon after. The electron fraction distribution follows the entropy distribution, with high \( Y_e \) (\( Y_e > 0.53 \)) concentrated along the outer cusps of each plume (see §3.4). We see high-\( Y_e \) material in both plumes as well as in the interior.

We show in Fig. 2 a volume rendering of the entropy per baryon showing the morphology of the explosion of the 11-M$_\odot$ progenitor from Sukhbold et al. (2018) from an upcoming paper (Radice et. al, 2018). The snapshot is taken at \( \sim 690 \) ms after bounce, when the shock wave (blue outer surface in the figure) has an average radius of \( \sim 3500 \) km. The explosion behaves similarly to that of the 16-M$_\odot$ progenitor we evolve. The shock is expanding quasi-spherically; however, accretion continues on one side of the PNS, while neutrino-driven winds inflate high-entropy bubbles on the other side.

In Fig. 3, we illustrate a time sequence of entropy slices for the 3D simulation of the 16-M$_\odot$ progenitor along the x-y plane (top). At early times, shock breakout is driven by multiple smaller bubbles in 3D, as opposed to a few large plumes in 2D. The shock evolution in 3D transitions from quasi-spherical expansion to expansion along an axis, with the axis randomly chosen. By \( \sim 300 \) ms after bounce, the plumes in 3D have merged into two distinct larger-solid-angle bubbles oriented along a clear axis. We see matter cross and accrete through this axis at earlier times before the explosion settles into the final configuration (see panels 3-5 of Fig. 3). At late times in the 3D simulation, we see the larger plume growing relative to the smaller, leaving a dominant driving plume. This is similar to the behavior in 2D. A persistent wind that emerges \( \sim 300 \) ms after bounce is present in both the large and small explosion plumes, and finally in the dominant plume alone. We see simultaneous explosion and accretion – the smaller plume in Fig. 3 growing relatively in size. Even up to the end of our simulation, some material partially circumnavigates the explosion plumes, plunges inward in a sheet that seems to pinch off the larger from the smaller plume, and is accreted onto the PNS. This accretion pinching in the early explosion phase between the two differently-sized exploding plumes resembles a wasp’s waist and may be a common feature of some CCSN explosion morphologies. The smaller plume is more prominent in 3D than in 2D, for which at late times the opposing explosion plume’s volume ratio is significantly smaller than in 3D.

An inner structure with two counter-ejected large lobes such as we see in this simulation, with one demonstrably larger than the other, crudely resembles the iron ejecta pattern inferred from XMM X-ray observations of the supernova remnant (SNR) Cas A (Willingale et al. 2003). This is suggestive, but the remnant structure in any SNR depends upon its entire propagation history through the star’s matter field and any apparent morphological association between early and late ejecta patterns could be happenstance. This remains to be determined. However, the rough similarity between our preliminary debris field morphology and the inferred inner mass density and composition patterns from X-ray data is indeed intriguing.

The 3D simulation has lower maximum entropies at late times by \( \sim 4.5 \) units (Boltzmann constant (\( k_B \)) per baryon) than its 2D counterpart. However, the entropy averaged over the shocked region (defined where the specific entropy is greater than \( 4 \text{ kg} \) per baryon) is comparable for both simulations. This is because the 3D simulation maintains a more ‘isotropic’ explosion in that even the subdominant plume subsists, producing comparable mean entropies over the shocked region despite the higher entropies along the dominant axial plume in 2D.

3.1 Shock Wave Evolution

We find, perhaps surprisingly (Hanke et al. 2012, 2013; Do- lence et al. 2013) that our 3D model explodes roughly 50 ms earlier than the corresponding 2D model. In the top panel of Fig. 4, we plot the shock radius versus time after bounce for the 2D (dashed, blue swath) and 3D (solid, green swath). The colored-in areas indicate the radial spread of the shock location, from minimum to maximum. At the end of our 3D simulation, the mean shock radius has reached beyond \( \sim 5000 \) km. The 2D model remains roughly spherical in expansion for the first \( \sim 120 \) ms, whereas the 3D model deviates from spherical symmetry earlier. We show in the inset a zoomed-in plot of the average shock radii at early times. The shock radii for the 2D and 3D simulations diverge around \( \sim 50 \) ms.
after bounce. The shock of the 3D model barely stalls, while the shock for its 2D counterpart stalls for \( \sim 50 \) ms.

In the bottom panel of Fig. 4, we plot the first four spherical harmonics of the shock radius as a function of time after bounce. We take the norm over all orders \( m \) and compare 3D (solid) with 2D (dashed). We use the approach outlined in Burrows et al. (2012) to decompose the shock surface \( R_\theta(\theta, \phi) \) into spherical harmonic components with coefficients:

\[
a_{lm} = \left( \frac{-1}{4\pi} \right)^{1/2} \int_0^{2\pi} \int_0^\pi R_\theta(\theta, \phi) Y_l^m(\theta, \phi) d\Omega,
\]

(1)

normalized such that \( a_{00} = a_0 = \langle R_\theta \rangle \) (the average shock radius) and \( a_{11}, a_{1-1} \), and \( a_{10} \) correspond to the average Cartesian coordinates of the shock surface \( \langle x_1 \rangle, \langle y_1 \rangle \), and \( \langle z_2 \rangle \), respectively. The orthonormal harmonic basis functions are given by

\[
Y_l^m(\theta, \phi) = \begin{cases} \frac{\sqrt{2} N_l^m P_l^m(\cos \theta) \sin m\phi}{\sqrt{2\pi}} & m > 0, \\ \frac{N_l^0 P_l^0(\cos \theta)}{\sqrt{2\pi}} & m = 0, \\ \frac{\sqrt{2} N_l^{-m} P_l^{-m}(\cos \theta)}{\sqrt{2\pi}} & m < 0, \end{cases}
\]

(2)

where

\[
N_l^m = \sqrt{\frac{2l + 1}{4\pi} (l - m)! (l + m)!},
\]

(3)

\[ P_l^m(\cos \theta) \] are the associated Legendre polynomials, and \( \theta \) and \( \phi \) are the spherical coordinate angles. We plot the norm,

\[
P_l^m = \frac{\sum_{n=-l}^{l} a_{nm}^2}{a_{00}}.
\]

(4)

Up to \( \sim 70 \) ms after bounce, the \( l = 2,4 \) moments dominate, the former due to the initial quadrupolar velocity perturbations imposed. From \( \sim 100 \) to \( \sim 200 \) ms, all moments are comparable in magnitude. Note that the dip in the quadrupole moment at \( \sim 300 \) ms corresponds to the dip in mean shock radius seen in the left panel. Shortly afterwards, the shock surface of the 2D simulation rapidly expands, catching up with that of the 3D simulation. At late times, the large-scale, lower \( l \) moments dominate. Up to \( l = 11 \) (not shown), we find that the moment magnitudes decrease monotonically with increasing \( l \) (and decreasing angular scale). We witness a transition from small structures at early times, coalescing into large-scale structures at later times. As the explosion commences, the 3D simulation evinces larger deviations from spherical symmetry than the 2D simulation, as indicated by the larger magnitudes of the respective moments. However, at late times the 2D simulation begins to manifest larger asymmetries than its 3D counterpart, indicated by the larger magnitude of the lower-order moments. Both simulations have similar asymptotic shock velocities and maximum shock radii (at a given post-bounce time), though the 2D simulation minimum and average shock radii are roughly \( \sim 1000 \) km smaller.

In Fig. 6, we track the dipole orientation of the shock with time. Early on, the shock dipole vector changes sporadically (but does not simply jump up and down as in 2D), but at later times it settles to an axis seemingly chosen arbitrarily. The randomly chosen axis is a defining feature of 3D non-rotating simulations (see, e.g. Fig. 3 in Burrows et al. 2012). We also see pronounced azimuthal structures in the 3D simulation (as opposed to rings in 2D). Along with the \( \ell = 0 \) explosion mode, the \( \ell = 1, m = \pm 1 \) dipolar mode dominates at late times, and we see such a structure in the 3D explosion maps (Fig. 1).

3.2 Energetics

Before explosion, the energy deposited in the gain region, that thick shellular volume interior to the shock wave where neutrino heating rate exceeds the cooling rate, is most relevant for driving turbulence and establishing the potential for explosion. The larger the energy deposition rate, the closer a given progenitor model is (with its mass accretion rate) to explosion (Burrows & Goshy 1993). However, the total energy deposited in advance of explosion is not related to the explosion energy (Burrows et al. 1995). The matter heated in the gain region is subsequently advected into the PNS, where it first reradiates a fraction of the acquired energy and then merges with the radiating PNS. It is only after the explosion commences that the deposited energy might be retained to contribute to the asymptotic explosion energy. However, even though explosive expansion leads to diminished cooling as the matter temperatures decrease, there continues to be some neutrino cooling. More importantly, the exploding matter expands against gravity, so that much of the ongoing neutrino energy deposited is used to lift the matter out of the deep potential well. This explains why the neutrino heating rates even during explosion are larger than the accumulation rate of the supernova blast energy in the first seconds of the explosion phase. Recombination of the nucleons into nuclei will provide a boost (~9 MeV per baryon) to the asymptotic kinetic energy of the supernova ejecta, but the associated recombining mass is generally not large (here \( \sim 0.08 \, M_\odot \)). Moreover, the associated total energy is comparable to the gravitational binding term. As a result, it appears that the supernova will take many seconds to achieve its final energy. Therefore, even though our 3D simulation of this 16-M_\odot progenitor’s core has been conducted farther post-bounce than any other simulation with state-of-the-art numerics and microphysics, we have captured only the early stages of an explosion that will need to be followed numerically for a few more seconds to witness the asymptoting of the explosion energy (Müller 2016; Müller et al. 2017).

The total energy we plot in Fig. 6 is comprised of the kinetic energy, the thermal energy, the recombination energy, and the gravitational energy of the ejecta. The so-called “diagnostic” energy ignores the binding energy (thermal plus gravitational) of the progenitor exterior to the computational domain. Here, the total energy quoted includes this penalty, different for every progenitor and outer computational boundary radius; including this term is required to assess the true supernova explosion energy.

We calculate diagnostic energies for our 16-M_\odot progenitor in 3D and 2D, summing the kinetic, thermal, gravitational, and nuclear binding energies interior to our 10,000-km simulation grid where the matter parcel’s Bernoulli term is positive. We correct for the gravitational binding energy of 2.5\times10^{50} erg exterior to our grid, and plot both the diagnostic (blue) and net (black) explosion energies in the left panel of Fig. 6. In the right panel, we plot the thermal (blue, left y-axis), gravitational (red, left y-axis) and kinetic (green, right y-axis) energies (in 10^{50} erg) as a function of time af-
The 3D model explodes slightly earlier and initially has a higher explosion energy than its 2D model counterpart (Fig. 6). At the end of the simulation, 677 ms after bounce, the 3D model has a diagnostic explosion energy of \(1.7 \times 10^{50}\) erg, whereas the 2D model has a total explosion energy (blue) of \(-0.8 \times 10^{50}\) erg. Before \(-550\) ms after bounce, the 3D model simulation maintains similar kinetic energies and a higher internal energy by \(-15\%\) than its 2D analog. Thenabouts, the 2D model explosion energy overtakes that of the 3D model, with the rise in explosion energy corresponding to a steep rise in its kinetic energy at a growth rate of \(\sim 5 \times 10^{50}\) erg s\(^{-1}\). Such a rise, also at \(-550\) ms after bounce, is seen in Vartanyan et al. (2018) for the same 16-M\(_{\odot}\) progenitor, but with a different initial setup. It is not seen in our 3D simulation. We conjecture that the stronger dipole and quadrupole moments of the 2D simulation (Fig. 4, right) relative to those of the corresponding 3D model at late times contribute to this divergence in kinetic energy. At the end of our simulation, the explosion energy for the 3D model is climbing at a rate of approximately \(2.5 \times 10^{50}\) erg s\(^{-1}\), half that of the 2D case. Similar energy growth rates are found for the 3D simulations in the literature (see, e.g. Müller et al. 2017) and necessitate continuing 3D simulations for several seconds.

In Fig. 7, top panel, we illustrate the heating rates and the gain mass as a function of time after bounce for the 3D (solid) and 2D (dashed) simulations of the 16-M\(_{\odot}\) progenitor. Just prior to explosion, at \(-100\) ms, the heating rate for the 3D simulation is \(-30\%\) (2 Bethe s\(^{-1}\)) higher than for the corresponding 2D model. The gain mass is also slightly higher for the 3D model, exceeding \(0.12\) M\(_{\odot}\) at the end of our simulation. After \(-150\) ms post-bounce, we see more variability in the heating rate for the 2D simulation than for the 3D simulation. Through almost \(-700\) ms after bounce, the growth rate of the explosion energy is less than \(-20\%\) of the heating rate, the difference due to the work done against gravity by the ejecta. It is not until late times that the growth rate of the explosion energy is expected to be close to the heating rate. In the middle panel, we show the spread of the inner boundary of the gain region as a function of time after bounce, defined here where the net heating (heating minus cooling) is greater than 10\% of the heating alone. The 3D simulation (green, solid) maintains a much larger variation in radial boundary throughout the evolution, extending almost twice as far at late times as the 2D model. In the bottom panel, we show the heating efficiency \(\eta\), defined as the heating rate divided by the luminosity entering the gain region,

\[
\eta = \frac{\dot{Q}_{\text{heat}}}{L_{\nu_e} + L_{\nu_\mu}}. \tag{5}
\]

Through the first \(-150\) ms, the 3D simulation has a heating efficiency of \(-0.09, 40\%\) higher than the corresponding 2D model. However, after \(-200\) ms, the efficiency of the 2D simulation overtakes that of the 3D simulation, and showcases a high degree of variability with a time scale of \(-50\) ms.

In Fig. 9, we show Mollweide projections of the accretion rate for the 3D and 2D models. The spatial variations for the 3D simulation for the accretion rate contrast sharply with that for the 2D simulation, in which we see a dominant dipole component only in the southern hemisphere.

### 3.3 Luminosity and Mean Energies

In Fig. 8, we plot the luminosity (top) and mean energies (bottom) at a radius of 500 km as a function of time after bounce. Note that the luminosities and average energies for the 2D and 3D models are remarkably similar and show significant difference only beyond \(-600\) ms after bounce. We note, however, key differences in the electron-neutrino luminosities through the first \(-150\) ms, with the 2D simulation boasting a luminosity \(-7\%\) larger than that for the 3D simulation. Furthermore, the ‘heavy’-neutrino luminosity is \(-3\%\) smaller for the 2D simulation than for the 3D simulation over the same time period. We explore this more in Sec. 3.5. Here, we remark that the interplay between the greater ‘heavy’ neutrino luminosity and the smaller ‘heavy’ neutrino luminosity in the critical first one-hundred ms of our 2D simulation (compared to our 3D model) impede earlier explosion revival in the 2D case. The former strips the gain region of energy deposition by neutrinos (since the electron-type neutrinos have a much higher absorption opacity than the ‘heavy’-type neutrinos). Furthermore, the greater ‘heavy’-neutrino luminosity in the 3D simulation may act in the same direction as the axial-vector many-body correction to produce a harder electron-neutrino spectrum and facilitate explosion (Burrows et al. 2018). The culmination of these effects is visible in Fig. 7, top panel, where a small difference in the respective luminosities translates into a significantly smaller heating rate in the 2D simulation compared to the analogous 3D simulation.

### 3.4 Ejecta Composition

Our calculations follow the evolution in space and time of the electron fraction, \(Y_e\). This quantity is an essential determinant of subsequent nucleosynthesis. While we do not in this paper derive the detailed elemental composition of our ejecta, the distributions of the entropies and \(Y_e\) in the inner explosion debris provide qualitative information on the likely character of the emergent element burden. In our previous 2D simulations (Vartanyan et al. 2018), histograms of the ejecta \(Y_e\) were derived. What we found was that much of the ejecta have \(Y_e\)'s above 0.5, implying that the ejected matter has been processed by differential \(\nu_e\) and \(\bar{\nu}_e\) absorption that has made some of it proton-rich. This is what we witness in this 3D simulation, though whether this is a generic outcome remains to be determined. Proton-rich ejecta could be a site of the p- and vp-processes (Pruet et al. 2006; Fröhlich et al. 2006; Wanajo et al. 2011) and might be the context for the production of some of the first peak of the r-process (Hoffman et al. 1996; Pruet et al. 2006; Fröhlich et al. 2006; Wanajo et al. 2011; Frebel 2018; Bliss et al. 2018).

In Fig. 10, we provide a histogram of the ejecta mass distribution in \(Y_e\) at 0.529 seconds after bounce. The green bars indicate the results of the 3D simulation, and the blue bars that of the 2D simulation. Though both models peak at \(Y_e = 0.5\), we find the interesting result that the ejecta distribution in the 2D model has a wider tail extending out...
to both higher ($>0.55$) and lower ($<0.5$) $Y_e$ than the 3D simulation at any given time. For much of the evolution, the ejecta of the 3D simulation spans $Y_e \sim 0.5-0.55$, whereas the ejecta in the 2D simulation encompasses $Y_e \sim 0.45-0.6$. Only at late times does the 3D simulation have significant low-$Y_e$ ejecta at large radii (see the violet tail in Fig. 11). 2

In an earlier paper on 2D models (Vartanyan et al. 2018), we found that only the 16-M$_\odot$ progenitor had an ejecta-$Y_e$ distribution that extended to lower $Y_e$, among the four progenitors considered. We claimed that an anisotropic explosion, with much of the outflow directed toward one hemisphere, would leave the opposite hemisphere with relatively untouched neutron-rich material. We see a similar result here. The 3D simulation, on the other hand, produces a more omnidirectional explosion – leaving little matter untouched. The achievement of higher $Y_e$ in 2D can similarly be understood – the concentration of explosion in one direction in the 2D simulation allows ample neutrino processing of the ejecta to higher $Y_e$.

We illustrate the 3D distribution of $Y_e$ in the ejecta in Fig. 11 at ~667 ms after bounce. The white “veil” illustrates a $Y_e$ of 0.5, just interior to the location of the shock radius. The high-$Y_e$ plumes correspond to the high-entropy plumes of Fig. 1, with the blue plumes indicating $Y_e$’s that span 0.5 ~ 0.52, and the red blobs $Y_e$ greater than 0.52. The latter is concentrated along the exterior cusps of the plumes, and in the interior where accretion is funneled onto the PNS. Note the resemblance of the high-$Y_e$ distribution in Fig. 11 to the entropy distribution in Fig. 1.

3.5 Inner PNS Convection

The original delayed explosion mechanism of Wilson (1985) was facilitated by the enhancement of the driving neutrino luminosities by what he termed “neutron-finger” convection. This was a doubly-diffusive instability, akin to salt-finger convection in the oceans, that was suggested to result in an otherwise stably-stratified PNS. A Ledoux-stable balance of $Y_e$ and entropy gradients was thought to be undermined by the more rapid diffusion of energy via viscosity or lepton number.

Wilson captured this effect in 1D spherical models of explosion with a mixing-length-like diffusive flux, and the $\nu_e$ and $\bar{\nu}_e$ luminosities were thereby augmented by ~25%. Without this effect, Wilson’s models did not explode. However, Bruenn & Dineva (1996) showed that the core was not unstable to such “neutron-finger” convection, and this was confirmed by Dessart et al. (2006) using 2D simulations. However, after bounce, there is a region in the PNS between ~10 and ~30 kilometers that is in fact unstable to classical convection, driven mostly by negative $Y_e$ gradients. This PNS convection is a feature in all modern multi-dimensional simulations of CCSNe. In their study, Dessart et al. (2006) noticed that this overturning convection increased the emergent luminosities, but by the end of their simulation ~200–300 ms after bounce this increase was not large. In addition, inner PNS convection and the outer neutrino-driven convection interior to the stalled shock did not merge into one large convective zone. Given this, Dessart et al. (2006) concluded that PNS convection was not centrally important to the neutrino mechanism of CCSNe.

On the contrary, in their study of the lowest-mass progenitor stars, Radice et al. (2017) found that the contribution of a PNS convection boost to the emergent neutrino luminosities grew with time after bounce, and could reach significant fractions. This was particularly true for $\nu_e$ and $\nu_\mu$ neutrinos, for which the respective neutrinospheres are deepest. Here, we explore the corresponding effects and numbers for our 3D simulation of the 16-M$_\odot$ progenitor of Woosley & Heger (2007), and compare them to the 2D case.

We plot in Fig. 12 the PNS mass (in M$_\odot$, blue) and mean radius (black) as a function of time after bounce for the 3D (solid), 2D (dashed), and 1D (red) simulations of the 16-M$_\odot$ progenitor. The PNS surface here is defined where the density is 10$^{11}$ g cm$^{-3}$. The baryonic PNS mass in our 3D simulation at ~677 ms after bounce is ~1.57 M$_\odot$ (1.6 M$_\odot$ in the 2D model, 1.63 M$_\odot$ in the 1D model), corresponding to a gravitational mass of 1.42 M$_\odot$ (1.44 M$_\odot$ in the 2D model, 1.47 M$_\odot$ in the 1D model). The PNS mass reflects the disruption of net accretion onto the PNS. Interestingly, we find that the difference between the PNS mass for the 1D and 2D models is roughly comparable to the difference in the same quantity between the 2D and the 3D models at late times, despite the absence of explosion in the 1D model and the correspondingly longer accretion history. Furthermore, at late times, the mean PNS radii in the 2D and 3D simulations are virtually identical (~29 km) but are significantly smaller in the 1D case (~23 km). A similar dependence of the PNS radius on simulation dimension was found in Radice et al. (2017) and Vartanyan et al. (2018). Here, we have the opportunity to compare such quantities to that of a 3D simulation. In the inset, we show the PNS radius zoomed in for the first 150 ms after bounce. Until ~140 ms after bounce, the PNS radius in the 2D simulation is as much as ~3% smaller than in the 3D model, lying between the PNS radii in the 3D simulation and in the 1D simulation. Simultaneously, as shown in Fig. 8, the “heavy”-neutrino luminosity is slightly smaller in the 2D simulation than in the 3D simulation. At later times, both the “heavy”-neutrino luminosity and the PNS radius in the 1D simulation are significantly lower than in the multidimensional simulations (see also Radice et al. 2018; Vartanyan et al. 2018). On time scales greater than ~200 ms, PNS convection boosts the “heavy”-neutrino luminosities in the 2D and 3D simulations. Furthermore, the shrinking PNS radius comes into close contact with the inner convective region after 200 ms (see Fig. 13), explaining the larger PNS radii in multi-dimensional simulations. However, electron-type neutrino luminosities are higher in 1D than in multidimensional simulations simply because that model does not explode, and accretion power remains significant.

In Fig. 13, we provide a space-time diagram of the standard deviation over angle of the radial velocity within the inner 100 km through 300 ms after bounce for the 3D (left) and 2D (right) models. Both convective regions are visible here as the bright regions – the interior convective band is similar to that seen in Dessart et al. (2006), and the exterior, neutrino-driven convection recedes to ~50 km by ~300 ms.
The interior convective zone in the 2D simulation is a few kilometers wider and has higher convective velocities than its 3D counterpart. Furthermore, we see more variation in the radial location of the convective zones in the 2D simulation. However, in the 3D simulation, the exterior, neutrino-driven convective region is located deeper in at early times, reaching ∼80 km by ∼50 ms after bounce in the 3D simulation (by comparison, the exterior convective region in the 2D case reaches 80 km more than 100 ms after bounce). Through the first ∼150 ms, this exterior convection reaches down into the PNS region in the 3D (but not the 2D) simulation. This may explain the slightly increased neutrino luminosities and shock radii in the 3D simulation seen in Fig. 8 and Fig. 12 at these earlier times. Lastly, we see a turbulent “teardrop” in the 3D simulation extending from ∼20 to ∼80 km in the first ∼40 ms after bounce, trailing off to both the inner and outer convective regions by ∼60 ms after bounce. By comparison, this feature is much smaller in extent and delayed to ∼40 ms after bounce in the 2D model. The PNS convective zone has a characteristic size of ∼10 km, a turnover time of ∼10 ms, and convective velocities of ∼1000 km s$^{-1}$. This is a manifestation of the stronger turbulence within 100 km at early times in the 3D simulation.

We explore the convective differences in the 2D and 3D simulations in Fig. 14. We show velocity vectors (white) on a $Y_e$ colormap depicted on an x-y slice of the 3D simulation (left) and an x-z slice of the 2D simulation (right) at ∼57 (top), ∼304 (middle), and ∼667 (bottom) ms after bounce to illustrate the evolution of inner PNS convection. The vectors lengths are scaled to velocity and made to saturate at 2000 km s$^{-1}$. Note the characteristic whorls forming within the first ∼60 ms after bounce.

3.6 On the Possible Presence of the LESA and the SASI

The lepton-number emission self-sustained asymmetry (LESA) was proposed in Tamborra et al. (2014) as a neutrino-hydrodynamical instability resulting in $\nu_e - \bar{\nu}_e$ asymmetry. In an earlier work (Vartanyan et al. 2018), we explored the possibility of LESA by examining the dipole harmonic component, $a_{\ell\ell}$, of the net lepton number flux. In that paper, we concluded that, at least in 2D, the effect was negligible and speculated that the inference of LESA may be a consequence of the use of the ray-by-ray approximation to multi-dimensional neutrino transport.

We now extend our exploration of the possible presence of the LESA, using for the first time an exploding 3D model with full physical realism. In Fig. 15, we depict the monopole and dipole components of the lepton asymmetry ($F_{\nu_e} - F_{\bar{\nu}_e}$) as a function of time after bounce at 500 km for both our 3D and 2D simulations. Here, we follow O’Connor & Couch (2018) and plot instead the dipole magnitude,

$$A_{\text{dipole}} = 3 \times \sqrt{\frac{1}{i=1} a_{\ell\ell}^2},$$

using the normalization scheme of Burrows et al. (2012). The net effect is to increase the strength of the dipole term relative to the monopole term by a factor of ∼1.73 (3/$\sqrt{3}$). We conclude that we do indeed find a LESA (see also O’Connor & Couch 2018) effect, and that (at least for these models) it is stronger in 3D than in 2D. However, the magnitude of the fluctuations in the lepton asymmetry is larger in 2D than in 3D. In addition, whereas Tamborra et al. (2014) find that the dipole term overtakes the monopole term as early as ∼200 ms after bounce, we find that only after ∼650 ms after bounce does the dipole component of the LESA become comparable to the monopole term. We continue to suggest that the ray-by-ray approach leads to a larger LESA, but this remains to be tested with a comparison of 3D ray-by-ray and multi-angle simulations.

We have also studied our 3D simulation for the possible presence of the standing accretion shock instability (SASI) (Blondin et al. 2003) during any phase of its evolution. If present, this should manifest in a narrow and obvious frequency peak in various power spectra. Recent work in 3D (Walk et al. 2018) found pronounced peaks in the electron anti-neutrino power spectrum at ∼60 and ∼110 Hz that the authors associated with the SASI. In addition, Kuroda et al. 2017 and Kuroda et al. 2016b suggested that softer equations of state manifest the SASI, with its gravitational wave signature lasting for an interval of ∼100 ms (a fraction of their simulation time) at frequencies of ∼50-200 Hz. Figure 16 portrays the Fourier decomposition of the dipole moment of the shock radius in both our 3D simulation and the associated 2D simulation out to 200 ms after bounce. We find no clear peak at these frequencies, either by this metric or in the gravitational wave emissions (not shown here). Moreover, a glance at Fig. 4 reiterates that we see in the 3D run no significant dipole term in the shock radius until after explosion. 3 Therefore, we conclude that we have no evidence for the SASI in our 16-M$_\odot$ simulations. However, since we find an early explosion in both the 3D and 2D simulations, perhaps the SASI may have had insufficient time to develop. It is important to note, however, that O’Connor & Couch (2018) likewise did not see a SASI for their 3D simulation (which was carried out to ∼600 ms after bounce, and did not explode) of a 20-M$_\odot$ progenitor when incorporating velocity dependence. Note that the small bump at ∼40 Hz in Fig. 4 corresponds to small-amplitude oscillations of the shock dipole in the first ∼100 ms after bounce. This feature is easily associated with the characteristic large-scale advective and convective time scales in the region between the shock and the PNS.

We summarize here some of the catalysts to explosion in 3D. The 16-M$_\odot$ progenitor model (Woosley & Heger 2007) upon which we focus in this paper has a steep density dropoff interior to 1.7-M$_\odot$ due to its Si-O interface. Such a sharp density drop has been shown to facilitate explosion in models incorporating turbulence (be they 2D or 3D) (Vartanyan et al. 2018) and we witnessed the explosion of this model in our previous 2D study. In addition, our inclusion of the many-body effect on the neutrino-nucleon scattering cross sections (Burrows et al. 2018) and the introduction of the significant velocity perturbations to the progenitor are both conducive to explosion. These aspects, in addition to the effects of GR and heating due to inelastic neutrino-electron and neutrino-nucleon scattering, seem to be some of the agents of “success.”
4 CONCLUSIONS

We have presented in this paper one of the first non-rotating, state-of-the-art, full-microphysics simulations in three spatial dimensions to explode as a supernova. The explosion of a 16-M⊙ progenitor is fully underway by ∼200 ms after bounce and at the end of the simulation is accumulating energy at a rate that if continued would reach ∼0.5 Bethes (0.5 × 10^51 erg) within two seconds. However, what its final asymptotic energy will be remains to be seen. The gravitational mass of the remaining neutron star is ∼1.42 M⊙. The morphology of the emerging debris field has a roughly diplar structure, with two asymmetric wide-angle lobes (one large, one small), whose axis emerged randomly. Whether slight rotation would impose an axis for the ejecta, or what rotation rate would be necessary to bias the emergent explosion axis, is not here determined. By the end of the simulation, an exploding debris field is accompanied by simultaneous inward accretion between the expanding lobes of some of the inner-progenitor matter, partly responsible for maintaining a driving neutrino luminosity (Burrows et al. 2007a). Interestingly, the majority of the ejecta of this supernova are proton-rich, with Y_e between 0.5 and 0.56. This will have interesting consequences for the associated nucleosynthesis, with the potential to explain in part the first r-process peak with modern codes such as FORNAX and energy-group resolutions. In 3D, a resolution study, even encouraging, there remain a number of important caveats. Important among these are the dependence upon the spatial distributions to both the neutral-current and the charged-current equations of state is dwindling, the EOS dependence of the neutrino-driven turbulence (Burrows et al. 1995; Herant et al. 1994), the net effects of general relativity (Bruenn et al. 2001), the inclusion of inelastic scattering and energy redistribution via neutrino-electron and neutrino-nucleon scattering (Burrows et al. 2018; Vartanyan et al. 2018; Just et al. 2018), the many-body correction to neutrino-nucleon scattering (Burrows & Sawyer 1998; Horizon et al. 2017; Burrows et al. 2018), the accretion of a sharp silicon-oxygen interface at a propitious time (Vartanyan et al. 2018), and the imposition of velocity perturbations in the progenitor. A major consequence of the many-body correction is the decrease in the scattering rate that increases the neutrino emission rates. This is particularly true for the ν_e,ν_ and the resulting acceleration of core contraction leads to, among other things, the increase in the temperatures around the ν_e,ν_ and ν_ neutrinospheres. This leads to a slight hardening of the emergent ν_e,ν_ spectra and an increase in the heating rate due to charged-current absorption on the free nucleons in the gain region. One of the most important future classes of investigations of direct relevance to the CCSN mechanism is the magnitude and role of many-body corrections to both the neutral-current and the charged-current (Burrows & Sawyer 1999; Roberts et al. 2012; Roberts & Reddy 2017) neutrino-matter interaction rates. We note as well that even though the number of viable published nuclear equations of state is dwindling, the EOS dependence of the outcome of collapse has not been definitively addressed, nor well explained. This will be a necessity in the years to come as laboratory constraints become ever more stringent.

While the results presented in this paper are quite encouraging, there remain a number of important caveats. Important among these are the dependence upon the spatial and energy-group resolutions. In 3D, a resolution study, even with modern codes such as FORNAX, is expensive, but will be necessary to determine both the quantitative and qualitative limitations of what we have presented here. The chaotic character of turbulent flow will make this a challenging en-
deavor for the community going forward. Moreover, we have conducted these calculations including the effects of general relativity in approximate fashion (§A). Doing these calculations with full GR will be important and attempts in this direction have already been made (Roberts et al. 2016; Ott et al. 2018; Kuroda et al. 2018). To enable these forefront simulations, we still had to make approximations in the neutrino sector. Foremost among these is the use of the moment formalism and an analytic closure for the second and third moments. While recent tests of the accuracy of such an approach in the core-collapse context are encouraging (Richers et al. 2017; O’Connor et al. 2018), solving the full Boltzmann equation with neutrino angles in the full six-dimensional phase space will require a significantly more capable national and international computational infrastructure. Finally, it has been shown that explodability when near criticality and in multi-D is a sensitive function of details in the neutrino-matter interaction rates (Burrows et al. 2018) in a way not seen in 1D simulations. This puts a premium on implementing correctly the correct microphysics. All models aspire to this goal, but whether we or others actually have achieved this is, or should be, a constant worry.

The model we presented was non-rotating. We think that most collapsing cores, while they are certainly rotating, are not generally rotating at rates sufficient to make a qualitative difference most of the time (Emmering & Chevalier 1989; Faucher-Giguère & Kaspi 2006; Popov & Turkola 2012; Noutsos et al. 2013). However, this remains to be exhaustively explored. Rapid rotation can certainly affect the outcome, both directly and by providing significant free energy to feed large magnetic fields and enable the direct effects of magnetic stress, when strong, on the explosion dynamics (see, e.g., Burrows et al. 2007b; Móstè et al. 2015). In fact, rapid rotation alone can affect the dynamics and facilitate explosion even when the expected magnetic field amplifications are ignored (Fryer & Warren 2002, 2004; Marek & Janka 2009; Summa et al. 2018). Moreover, rapid rotation can also generate a non-axisymmetric spiral-arm mode, which resembles the SASI in the rotating context and might enlarge the gain region and, thereby, facilitate explosion (Takiwaki et al. 2016; Summa et al. 2018). Curiously, if the explosion is suitably delayed, such a mode may also grow in the non-rotating context (Blondin & Shaw 2007; Rantsiou et al. 2011; Guilet & Fernández 2014; O’Connor & Couch 2018). This and other related issues are fruitful topics for future work.

However, we view the achievement of a 3D simulation that leads naturally to explosion, with competitive resolution, including all the relevant microphysics, using a state-of-the-art simulation tool, and calculating significantly post-bounce as a major milestone in the decades-long quest to resolve the core-collapse supernova puzzle in quantitative detail. What remains in the near term is to determine the progenitor mass dependence of the outcome of collapse in 3D, to understand the possible roles of rotation, to explain the supernova energies and neutron star masses observed, and to explain the morphologies of the debris fields seen in supernova remnants. Furthermore, a major motivation of all supernova simulations is the detailed explanation of the explosive production of the elements. The ejecta we find are mostly proton-rich, and this emerges naturally from the detailed simulations. What the consequences are of this finding will be one of the topics of our future studies as we continue our quest to understand one of the most persistent problems in stellar and nuclear astrophysics.

ACKNOWLEDGMENTS

The authors acknowledge helpful discussions with Todd Thompson regarding inelastic scattering, Evan O’Connor regarding the equation of state, and Gabriel Martínez-Pinedo concerning electron capture on heavy nuclei. We also acknowledge invaluable support from Viktornya Morozova with visualization using VisIt, and Sydney Andrews for helpful discussion and feedback. We acknowledge support from the U.S. Department of Energy Office of Science and the Office of Advanced Scientific Computing Research via the Scientific Discovery through Advanced Computing (SciDAC) program and Grant DE-SC0018297 (subaward 00009650). In addition, we gratefully acknowledge support from the U.S. NSF under Grants AST-1714267 and PHY-1144374 (the latter via the Max-Planck/Princeton Center (MPPC) for Plasma Physics). DR acknowledges partial support as a Frank and Peggy Taplin Fellow at the Institute for Advanced Study. The authors employed computational resources provided by the TIGRESS high performance computer center at Princeton University, which is jointly supported by the Princeton Institute for Computational Science and Engineering (PICSciE) and the Princeton University Office of Information Technology, and by the National Energy Research Scientific Computing Center (NERSC), which is supported by the Office of Science of the US Department of Energy (DOE) under contract DE-AC03-76SF00098. The authors express their gratitude to Ted Barnes of the DOE Office of Nuclear Physics for facilitating their use of NERSC. This overall research project is also part of the Blue Waters sustained-petascale computing project, which is supported by the National Science Foundation (awards OCI-0725070 and ACI-1238993) and the state of Illinois. Blue Waters is a joint effort of the University of Illinois at Urbana-Champaign and its National Center for Supercomputing Applications. This general project is also part of the “Three-Dimensional Simulations of Core-Collapse Supernovae” PRAC allocation support by the National Science Foundation (under award #OAC-1809073). Under the local award #TG-AST170045, our ongoing supernova efforts are enhanced through access to the resource Stampede2 in the Extreme Science and Engineering Discovery Environment (XSEDE), which is supported by the National Science Foundation grant number ACI-1548562. This work was performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344 and has been assigned an LLNL document release number LLNL-JRNL-757405. This work was performed under the auspices of the U.S. Department of Energy by Los Alamos National Laboratory under Contract DE-AC52-06NA25396 and has been assigned an LANL document release number LA-UR-18-28730. JD acknowledges support from the Laboratory Directed Research and Development program at Los Alamos National Laboratory.

MNRAS 000, 1–23 (0000)
D. Vartanyan et. al

Seadrow S., Burrows A., Vartanyan D., Radice D., Skinner M. A., 2018, MNRAS, 480, 4710
Shibata M., Kiuchi K., Sekiguchi Y., Suwa Y., 2011, Progress of Theoretical Physics, 125, 1255
Skinner M. A., Burrows A., Dolence J. C., 2016, ApJ, 831, 81
Skinner M. A., Dolence J. C., Burrows A., Radice D., Vartanyan D., 2018, preprint, (arXiv:1806.07390)
Steiner A. W., Hempel M., Fischer T., 2013, ApJ, 774, 17
Sukhbold T., Woosley S. E., Heger A., 2018, ApJ, 860, 93
Summa A., Janka H.-T., Melson T., Marek A., 2018, ApJ, 852, 28
Takiwaki T., Kotake K., Suwa Y., 2012, ApJ, 749, 98
Takiwaki T., Kotake K., Suwa Y., 2016, MNRAS, 461, L112
Tamborra I., Hanke F., Janka H.-T., Müller B., Raffelt G. G., Marek A., 2014, ApJ, 792, 96
Tews I., Lattimer J. M., Ohnishi A., Kolomeitsev E. E., 2017, ApJ, 848, 105
Thompson T. A., Burrows A., Horvath J. E., 2000, Phys. Rev. C, 62, 035802
Thompson T. A., Burrows A., Pinto P. A., 2003, ApJ, 592, 434
Vartanyan D., Burrows A., Radice D., Skinner M. A., Dolence J., 2018, MNRAS, 477, 3091
Vaytet N. M. H., Audit E., Dubroca B., Delahaye F., 2011, J. Quant. Spectrosc. Radiative Transfer, 112, 1323
Wallace J., Burrows A., Dolence J. C., 2016, ApJ, 817, 182
Wanajo S., Janka H.-T., Kubono S., 2011, ApJ, 729, 46
Willingale R., Bleeker J. A. M., van der Heyden K. J., Kaastra J. S., 2003, A&A, 398, 1021
Wilson J. R., 1985, in Centrella J. M., Leblanc J. M., Bowers R. L., eds, Numerical Astrophysics. p. 422
Woosley S. E., Heger A., 2007, Phys. Rep., 442, 269
Woosley S. E., Weaver T. A., 1995, ApJS, 101, 181
Woosley S. E., Heger A., Weaver T. A., 2002, Reviews of Modern Physics, 74, 1015

MNRAS 000, 1–23 (0000)
APPENDIX A: APPROXIMATE GENERAL RELATIVISTIC FORMULATION

As stated in Sec. 1, we use the M1 closure to truncate the radiation moment hierarchy by specifying the second and third moments as algebraic functions in terms of the zeroth and first. The basic equations of radiative transfer in the comoving frame that we solve are the zeroth- and first-moment equations of the full equation of radiative transfer for the specific intensity. For neutrino transfer, we currently follow the evolution of $\nu_e$, $\bar{\nu}_e$, and $\nu_x$ neutrinos, where the latter represents the $\nu_\mu$, $\bar{\nu}_\mu$, and $\nu_\tau$, neutrinos collectively. With explicit neutrino source and sink terms, the full set of Newtonian radiation/hydrodynamic equations, with a specific focus on the neutrino radiation implementation relevant to the study of core-collapse supernovae, are:

$$\rho_{,i} + (\rho v^i)_{,i} = 0,$$

$$\left(\rho v^i\right)_{,i} + (\rho v^i v_j + P \delta^i_j)_{,i} = -\rho \phi_{,j} + \epsilon^{-1} \sum_j \int_0^\infty (\epsilon_{SE} + \sigma_{\nu_j}^N) F_{SEj} \, dx,$$

$$\left[ \rho \left( e + \frac{1}{2} \|v\|^2 \right) \right]_{,i} + \rho v^i \left( e + \frac{1}{2} \|v\|^2 + P \right)_{,i} = -\rho v^i \phi_{,j} - \sum_j \int_0^\infty \left( j_{SE} - c \epsilon_{SE} E_{SE} - \frac{\epsilon}{c} (\epsilon_{SE} + \sigma_{\nu_j}^N) F_{SEj} \right) \, dx,$$

$$\left( \rho \chi_{,i} \right)_{,i} + (\rho v^i \chi)_{,i} = \sum_j \int_0^\infty \chi_{SE}(j_{SE} - c \epsilon_{SE} E_{SE}) \, dx,$$

$$E_{SE,i} + (F_{SE,i} + v^i E_{SE})_{,i} - v^j \frac{\partial}{\partial \ln E} P_{SEj}^{i} = j_{SE} - c \epsilon_{SE} E_{SE},$$

$$F_{SE,i} + (c^2 P_{SE,i}^{i} + v^i E_{SE})_{,i} + v^j P_{SEj}^{i} - v^j \frac{\partial}{\partial \ln E} (\epsilon Q_{SEj}^k) = -c (\epsilon_{SE} + \sigma_{\nu_j}^N) F_{SEj}.$$

where $\epsilon$ is the specific internal energy, $P = P(\rho, \epsilon, Y_e)$ is the pressure, $\rho$ is the mass density, $Y_e$ is the electron fraction, $v_i$ are the velocity components, $\epsilon_{SE}$ and $\sigma_{\nu_j}^N$ are the absorption and transport scattering opacities, and $s \in \{\nu_e, \bar{\nu}_e, \nu_x\}$, where

$$\begin{cases} \frac{-(N_A e)^{-1}}{s = \nu_e}, \\ \frac{(N_A e)^{-1}}{s = \bar{\nu}_e}, \\ 0 \quad s = \nu_x. \end{cases}$$

The corresponding radiation energy and momentum equations modified to approximately incorporate general relativistic effects are:

$$E_{SE,i} + (a F_{SE,i}^{i} + v^i E_{SE})_{,i} - a v^j \frac{\partial}{\partial \ln E} P_{SEj}^{i} = a j_{SE} - c \epsilon_{SE} E_{SE} + a G^e,$$

$$F_{SE,i} + (c^2 a P_{SE,i}^{i} + v^i E_{SE})_{,i} + a v^j P_{SEj}^{i} - a v^j \frac{\partial}{\partial \ln E} (\epsilon Q_{SEj}^k) = -a c (\epsilon_{SE} + \sigma_{\nu_j}^N) F_{SEj} + a G^m.$$

where differentiation is indicated with standard notation, $e$ is the neutrino energy, $s \in \{\nu_e, \bar{\nu}_e, \nu_x\}$, $E_{SE}$ is the radiation energy density spectrum (zeroth moment), $F_{SEj}$ is radiation flux spectrum (first moment), $P_{SEj}^{i}$ is the radiation pressure tensor (second moment), $Q_{SEj}^k$ is the heat tensor (third moment), $a = \exp(\phi/c^2)$, and the other variables have their standard meanings. $\phi$ is the gravitational potential.

$G^e$ and $G^m$ are the main terms to add in order to include gravitational redshifts (Rampp & Janka 2002; Shibata et al. 2011). They are given by

$$G^e = -F_{SE} \cdot \nabla \phi / c^2 + \nabla \phi / c^2 \cdot \partial (e F_{SE}) / \partial E,$$

$$G^m = -E_{SE} \nabla \phi + \nabla \phi \cdot \partial (e P_{SEj}^{i}) / \partial E,$$

where $\nabla \phi / c^2 = -\gamma / c^2$, and one must do the contravariant/covariant raising or lowering according to the metric. Notice that the last term in the equations for $G^e$ and $G^m$ integrate out to zero when one integrates over energy groups, leaving the terms analogous to the “$\gamma v \cdot \gamma$” and “$\gamma g$” work and force terms.

The gravitational potential, $\phi$, is generally taken to be the “GR-corrected” monopole term ($\phi_{TOV}$). There are a variety of ways to approximate this, and the source for this approximation is Marek et al. (2006). Many people use their “Case A,” as do we, though they say their “Case B” is also very good. The relevant equations are:
\[ \frac{d\phi_{\text{TOV}}}{dr} = G_{\text{TOV}} + 4\pi \Gamma \left( \frac{P + P_{\gamma}}{rc^2} \right) \left( \frac{\rho + E/c^2 + P/c^2}{\rho} \right). \]  
(A10)

\[ \Gamma(r) = \sqrt{1 + v_s^2/c^2 - \frac{2Gm_{\text{TOV}}(r)}{rc^2}}, \]  
(A11)

\[ \frac{d\phi_{\text{TOV}}}{dr} = 4\pi \left( \frac{\rho + E/c^2 + E_{\nu}/c^2 + \frac{v_s F_{\nu}/c^2}{\Gamma}}{\Gamma} \right) \]  
(A12)

\[ \frac{d\phi_{\text{TOV}}}{dr} = 4\pi \rho \quad \text{(Case B)}, \]  
(A13)

where \( \rho \) is the rest mass density, \( P_{\gamma} \) is the total neutrino pressure, \( E \) is the total matter internal energy density, \( P \) is the matter pressure, \( v_s \) is some averaged radial speed, \( E_{\nu} \) is the total neutrino energy density, and \( F_{\nu} \) is the total neutrino flux. If one is using a multipole expansion to derive the potential, then the potential used is:

\[ \phi_{\text{eff}} = \phi - \hat{\phi} + \phi_{\text{TOV}}. \]  
(A14)

where \( \phi \) is the multipole Newtonian potential, \( \hat{\phi} \) is the monopole Newtonian potential, and \( \phi_{\text{TOV}} \) is the monopole TOV potential. Note that this equation merely subtracts out the monopole term from the total Newtonian potential, and then adds it back, corrected for the GR effects in the approximate way suggested by Marek et al. (2006).

So, one needs to calculate the total pressure, energy density, and flux of the neutrinos, calculate \( (v_s^2/c^2) \) as a function of radius, and then integrate radially/spherically to get \( \phi_{\text{TOV}} \) and \( \phi_{\text{TOV}} \). All the non-monopolar potential contributions (if included) are Newtonian; only the monopole term is adjusted approximately for GR. This correction to the monopolar potential used in the matter momentum equation is likely the dominant effect of GR. However, the “GR-corrected” transport scheme above incorporates the neutrino energy redshifts, as well as the time dilation. In the steady-state, zero-motion limit, the total luminosity \( \times \exp(2\phi/c^2) \) is a constant, as it should be (note the factor of 2).

APPENDIX B: NEUTRINO-MATTER INTERACTIONS FOR THE SUPERNova PROBLEM

A comprehensive set of neutrino-matter interactions is implemented into FORNAX, and these are described in Burrows et al. (2006). They include neutrino-nucleon scattering and absorption and neutrino-nucleus scattering with ion-ion-correlations, weak screening, and form-factor corrections. For the neutrino-nucleon scattering cross sections, we use eq. 24 of Burrows et al. (2006) and for the charged-current absorption cross sections (i.e., \( \nu_e + n \rightarrow p + e^- \) and \( \bar{\nu}_e + p \rightarrow n + e^+ \)) we follow the approach described in sections 3.1 and 3.2 of Burrows et al. (2006). Emissivities are calculated to be consistent with Kirchhoff’s law of detailed balance, as described with eqs. 7 and 8 of Burrows et al. (2006). The latter incorporates the stimulated emission term for fermions, which in other formulations (cf. Brueg 1985) is equivalent to Pauli blocking.

The weak magnetism and recoil corrections for both absorption and scattering are incorporated as multiplicative factors, using the linear fits in neutrino energy of Horowitz (2002). The linear fits are accurate below \(~100\) MeV for \( \nu_e \)s and \(~50\) MeV for \( \bar{\nu}_e \)s, but deviate at higher neutrino energies. Nevertheless, higher-energy \( \nu_e \)s reside only in the core. Moreover, there are effectively no higher-energy \( \bar{\nu}_e \)s in the supernova core. The degeneracy of \( \nu_e \)s that results from lepton trapping also results in a positive \( \nu_e \) chemical potential, and, hence, a negative \( \bar{\nu}_e \) chemical potential. Such a negative potential exponentially suppresses \( \bar{\nu}_e \)s. Where the \( \bar{\nu}_e \)s can finally achieve significant occupancy, the temperatures and densities are too low to produce many \( \bar{\nu}_e \)s above \(~60\) MeV. The \( \nu_{\mu}, \nu_{\tau} \)s don’t experience such Boltzmann suppression, but are thermally produced, and, hence, given the core temperatures, are not produced in significant numbers above \(~100\) MeV. Be that as it may, we have also implemented the fully non-linear weak-magnetism and recoil formalism into FORNAX, done side-by-side comparison simulations in 1D, and found that the hydrodynamic and radiation results are almost identical. For the \( \nu_{\mu}, \nu_{\tau} \) neutrino-nucleus scattering, we use the average of the weak magnetism and recoil corrections for the neutrino and anti-neutrino types.

Inelastic neutrino-nucleon scattering is handled using a modified version of the Thompson et al. (2003) approach. A comprehensive discussion of the equations and techniques we employ to handle inelasticity in both neutrino-nucleon and neutrino-electron scattering is found in section 4 of Burrows & Thompson (2004). The integrals for the dynamic structure functions for inelastic neutrino-electron scattering are done numerically with quadratures, and the results are tabulated in large tables for use during simulation when inelasticity and redistribution are turned on (as they are in this work). This involves as an intermediate step the numerical calculation of polylogarithmic functions. Neutrino sources and sinks due to nucleon-nucleon bremsstrahlung and electron-positron annihilation are included, as described in Thompson et al. (2000). We also include the many-body correction to neutrino-nucleon scattering of Horowitz et al. (2017), which is a variation of the formalism of Burrows & Sawyer (1998) extended to lower densities. This correction, which slightly decreases the scattering rate at progressively higher densities, has been shown to support the “explodability” of supernova models and is physically well-motivated. A corresponding correction for charged-current absorption onto nucleons has not been calculated in full (Roberts & Reddy 2017), nor included in FORNAX, but could be of equal relevance. For electron capture on nuclei, of importance during the infall phase, we employ the rates of Juodagalvis et al. (2010).
Figure 1. Time sequence of the entropy of the 16-$\odot$ progenitor. Note the different spatial scales. The inner white sphere is a $10^{11}$ g cm$^{-3}$ isosurface that roughly delineates the PNS, and the blue veil traces an entropy contour of 4-kb/baryon, a proxy for the shock radius. Note the bifurcated cerebral structure of the explosion plumes, with one dominant hemisphere (on the left in this projection). Several “fingers” are also visible along the axis, though these are accreted shortly after. Note the high-entropy regions (dark red) both along the outer cusps of the plumes and in the interior as matter is funneled onto the PNS.

Figure 2. Volume rendering of the entropy per baryon showing the morphology of the explosion of the 11-$\odot$ progenitor from Sukhbold et al. (2018). The snapshot is taken at ~690 ms after bounce, when the shock wave (blue outer surface in the figure) has an average radius of ~3500 km. The shock is expanding quasi-spherically, however accretion continues on one side of the PNS, while neutrino-driven winds inflate higher-entropy bubbles on the other side.
Figure 3. Time sequence slices in the x-y plane illustrating the entropy of the 3D simulation of the 16-M⊙ progenitor. Note the changing spatial scales with time. At early times, shock expansion is driven by multiple bubbles, which coalesce into larger plumes. At approximately 300 ms after bounce, we note the development of a dividing axis with two dominant plumes in this slicing. At late times, a single dominant explosion plume emerges, seemingly at the expense of the secondary plume. A persistent wind is present in both plumes initially, and finally, only in the dominant plume. The secondary plume persists and grows, with a characteristic scale of ∼2000 km, half the size of the primary plume at the end of our simulation. We see simultaneous explosion and accretion. The shock evolution transitions from quasi-spherical expansion to axial expansion, with the axis arbitrarily chosen. See the text for a discussion.
Figure 4. Left: The shock radius (km) vs. time after bounce (in seconds) for the 2D (dashed, blue swath) and 3D (solid, green swath). The colored-in regions indicate the range of the shock location, from minimum to maximum. The 3D simulation explodes slightly earlier. At the end of our simulation, the shock achieves ~5000 km. The shock of the 3D model barely stalls in radius, while the shock for its 2D counterpart stalls for ~50 ms. We show in the inset a zoomed-in plot of the average shock radii at early times. The mean shock radii for the 2D and 3D simulations have diverged by ~50 ms after bounce. Right: The first four spherical harmonic moments of the shock radius as a function of time (in seconds) after bounce, normalized to the mean shock radius (the $l = 0$ component). We take the norm over all orders $m$ and compare 3D (solid) to 2D (dashed). Up to ~70 ms after bounce, the $l = 2, 4$ moments dominate, the former due to the initial quadrupolar velocity perturbations imposed. From ~100 to ~200 ms, all reduced moments are comparable in magnitude. At late times, the large scale, lower-$l$ moments increase in significance. Up to $l = 11$ (not shown), we find monotonically decreasing relative moment magnitudes with increasing $l$ (and decreasing angular scale). We see a transition from small structures at early times to large structures at later times. Up to explosion, the 3D simulation evinces much larger deviations from spherical symmetry. At late times, however, the 2D simulation shows much larger asymmetries than the 3D simulation, indicated by the larger magnitude of the reduced moments.

Figure 5. A Mollweide projection of the direction of the shock dipole as a function of time (in seconds) after bounce, color-coded. Early on, the shock dipolar direction is changes sporadically before settling at late times to a randomly chosen axis. See Fig. 3 of Burrows et al. (2012) for a comparison. Note that, in a 2D simulation, the dipole axis is required to lie along the z-axis; this is not the case in a 3D simulation.
Figure 6. Left: Diagnostic (blue) and net (black) explosion energies (in $10^{50}$ erg) for the 16-M$_\odot$ progenitor as a function of time after bounce (in seconds). Right: Internal (blue, left y-axis) and kinetic (green, right y-axis) energies (in $10^{50}$ erg) as a function of time after bounce (in seconds). Solid indicates the 3D model and dashed the corresponding 2D model for both figures. The diagnostic energy (left, green) does not account for the gravitational overburden of $\sim 2.5 \times 10^{50}$ erg exterior to our simulation grid (outer boundary 10,000 km). The total explosion energy (blue) is not yet positive for the 3D simulation (at 677 ms after bounce), though the 3D simulation explodes slightly earlier. The 3D simulation maintains a higher internal energy, by $\sim 15\%$, through the end of the simulation, and a higher explosion energy, but similar kinetic energies, until $\sim 550$ ms after bounce. The subsequent rise in explosion energy for the 2D model corresponds with the steep rise in its kinetic energy, also seen in Vartanyan et al. (2018) for the same 16-M$_\odot$ progenitor, but with a different initial setup. Such a sharp rise in kinetic energy is not seen in our 3D simulation.
3D CCSN Explosion

Figure 7. Top: We illustrate the heating rates (blue, $10^{51}$ erg s$^{-1}$), and the gain mass (black, in $10^{-3} M_\odot$) as a function of time after bounce (in seconds) for the 3D (solid) and 2D (dashed) simulations of the 16-$M_\odot$ progenitor. Prior to explosion ($\sim$100 ms), the heating rate for the 3D simulation is $\sim$30% higher than for the 2D simulation. The gain mass is also slightly higher for the 3D model, exceeding $0.12 M_\odot$ at the end of our simulation. Middle: Inner boundary of the gain region (in km) as a function of time after bounce (in seconds). Black lines depict the mean positions of the inner gain region (solid for 3D, dashed for 2D). The 3D simulation (green, solid) maintains a much larger variation of the inner boundary of the gain region throughout the evolution. Bottom: Heating efficiency $\eta$ (black), defined as the gain-region heating rate divided by the sum of the $\nu_e$ and $\bar{\nu}_e$ luminosities entering the gain region, and the accretion rate at 150 km (blue, in $M_\odot$ s$^{-1}$). Through the first $\sim$150 ms, the 3D simulation (green) has a heating efficiency $\sim$40% higher than the 2D (blue) simulation. However, after $\sim$200 ms, the 2D simulation overtakes the 3D simulation, and showcases a high degree of variability over $\sim$50-ms time scales. Note the correlation between jumps in accretion rate and jumps in heating rates (and efficiencies) in the 2D simulation.

Figure 8. Neutrino luminosity (top, $10^{51}$ erg s$^{-1}$), and average neutrino energy (bottom, MeV) as a function of time after bounce (in seconds) at 500 km. Note that the luminosities and average energies for 2D and 3D are remarkably similar and show a significant difference only after 600 ms after bounce.

Figure 9. Mollweide projections of the accretion rate for the 3D and the 2D simulations at 450 ms after bounce. The spatial variation of accretion rate in the 3D simulation is in sharp contrast with the accretion rate in the 2D simulation, where we see only a dominant dipole component in the southern hemisphere.
Figure 10. Histogram of ejecta mass distribution by $Y_e$ at 0.529 seconds after bounce. The green bars indicate the results of the 3D simulation, and the blue those for the 2D simulation. We find the interesting result that the ejecta mass distribution in 2D has a tail extending out to both higher ($> 0.55$) and lower ($< 0.5$) $Y_e$ than the 3D simulation at a given time.

Figure 11. $Y_e$ distribution at ~677 ms after bounce. The white “veil” encompasses the expanding plumes, just interior to the shock radius, at a $Y_e$ of 0.5. The blue plumes indicate a $Y_e$ spanning the interval 0.5 - 0.52, and the red caps a $Y_e$ greater than 0.52. The latter is concentrated along the exterior cusps of the plumes, and interior where accretion is funneled onto the PNS. Note the resemblance of the high-$Y_e$ distribution to the entropy distribution in Fig. 1. The violet tail shows the low-$Y_e$ (< 0.5) ejecta seen in Fig. 10. This trailing ‘tail’ is also visible in the density evolution of the progenitor.

Figure 12. The PNS mass (in $M_\odot$, blue) and radius (in km, black) as a function of time after bounce (in seconds) for the 3D (solid), 2D (dashed), and 1D (red) simulations of the 16-$M_\odot$ progenitor. At late times, the PNS radii for the 2D and 3D simulations are virtually identical, but significantly smaller in the 1D case. The larger PNS mass in 1D than 2D, and in 2D than 3D, is due to the longer accretion history than in 3D, where we see early explosion. In the inset, we show the PNS radius zoomed in for the first 150 ms after bounce. Until ~140 ms after bounce, the PNS radius in the 2D simulation is as much as ~3% smaller than for the 3D simulation.
Figure 13. A space-time diagram of the standard deviation \( \sqrt{\langle (v_r - \langle v_r \rangle)^2 \rangle} \) over angle of the radial velocity within the inner 100 km through 300 ms after bounce for the 3D (left) and 2D (right) models. Note that it is significantly smaller in 3D than in 2D (see also Fig. 14). Both the outer and inner (PNS) convective regions are visible here, and the interior convective zone is a band in velocity similar to that seen in Dessart et al. (2006). The black lines illustrate the mean PNS radius, which in 3D, and not 2D, is sampled by the outer neutrino-driven convection through the first 120 ms after-bounce. By \( \sim 300 \) ms after bounce, the exterior convective zone has receded to \( \sim 50 \) km. In the 2D simulation, the interior convective zone is a few km wider and has higher convective velocities by several hundred \( \text{km s}^{-1} \) than its 3D counterpart. Furthermore, we see more variation in the radial location of the convective zones in the 2D simulation, with the outer convective zone making excursions almost to the inner convective zone by \( \sim 300 \) ms after bounce. See the text for further discussion.
Figure 14. Velocity vectors (white) on a $Y_e$ colormap depicted on an x-y slice of the 3D simulation (left) and an x-z slice of the 2D simulation (right) at $\sim 57$ (top), $\sim 304$ (middle), and $\sim 667$ (bottom) ms after bounce to illustrate the evolution of inner-PNS convection. The velocity vector lengths are scaled to velocity and saturate at 2000 km s$^{-1}$. Note the characteristic convective whorls forming within the first $\sim 60$ ms after bounce. The region of inner convection (with $Y_e \sim 0.15-0.2$) shrinks with the PNS, and at later times the exterior, neutrino-driven convective region (with $Y_e \gtrsim 0.3$) is visible beyond $\sim 30$ km, with low-$Y_e$ “flares” traversing the boundary.
Figure 15. We plot the monopole (black) and dipole (blue) of net lepton number asymmetry $F_{\nu_e} - F_{\bar{\nu}_e}$ (in units of $10^{56}$ s$^{-1}$) as a function of time after bounce (in seconds) at 500 km to explore the possible appearance of the “LESA” phenomenon. Solid indicates the 3D model and dashed the 2D model. We do see the LESA effect, and the dipole term in the 3D simulation is larger and less variable than in the corresponding 2D model. However, the dipole term becomes comparable in magnitude to the monopole term only after $\sim$650 ms.

Figure 16. We plot the Fourier decomposition of the shock radius dipole component as a function of frequency (in Hz) for the first 100 ms after bounce for the 3D (dashed) and 2D (solid) simulations. Note that while the dipole component is insignificant for both models early on, it is larger for the 3D model during the first $\sim$100 ms. This is also as seen in Fig. 4 (solid red line, right panel).