| Publication Year | 2017 |
|------------------|------|
| Acceptance in OA@INAF | 2020-07-22T05:39:22Z |
| Title | The global mass functions of 35 Galactic globular clusters - II. Clues on the initial mass function and black hole retention fraction |
| Authors | Baumgardt, H.; SOLLIMA, ANTONIO LUIGI |
| DOI | 10.1093/mnras/stx2036 |
| Handle | http://hdl.handle.net/20.500.12386/26557 |
| Journal | MONTHLY NOTICES OF THE ROYAL ASTRONOMICAL SOCIETY |
| Number | 472 |
The global mass functions of 35 Galactic globular clusters – II. Clues on the initial mass function and black hole retention fraction

H. Baumgardt1* and S. Sollima2

1School of Mathematics and Physics, University of Queensland, St Lucia, QLD 4072, Australia
2INAF Osservatorio Astronomico di Bologna, via Gobetti 93/3, I-40129 Bologna, Italy

Accepted 2017 August 4. Received 2017 August 4; in original form 2017 June 1

ABSTRACT
In this paper, we compare the mass function slopes of Galactic globular clusters recently determined by Sollima & Baumgardt with a set of dedicated N-body simulations of star clusters containing between 65,000 and 200,000 stars. We study clusters starting with a range of initial mass functions (IMFs), black hole retention fractions and orbital parameters in the parent galaxy. We find that the present-day mass functions of globular clusters agree well with those expected for star clusters starting with Kroupa or Chabrier IMFs, and are incompatible with clusters starting with single power-law mass functions for the low-mass stars. The amount of mass segregation seen in the globular clusters studied by Sollima & Baumgardt can be fully explained by two-body relaxation driven mass segregation from initially unsegregated star clusters. Based on the present-day global mass functions, we expect that a typical globular cluster in our sample has lost about 75 per cent of its mass since formation, while the most evolved clusters have already lost more than 90 per cent of their initial mass and should dissolve within the next 1–2 Gyr. Most clusters studied by Sollima & Baumgardt also show a large difference between their central and global mass function (MF) slopes, implying that the majority of Galactic globular clusters are either near or already past core collapse. The strong mass segregation seen in most clusters also implies that only a small fraction of all black holes formed in globular clusters still reside in them.

Key words: methods: numerical – stars: luminosity function, mass function – globular clusters: general.

1 INTRODUCTION
This is the second of two papers in which we explore the present-day stellar-mass functions of Galactic globular clusters. In the first paper (Sollima & Baumgardt 2017), we derived completeness-corrected stellar-mass functions within the central 1.6 arcmin of 35 Galactic globular clusters based on Hubble Space Telescope (HST)/ACS data obtained as part of the Globular Cluster ACS Treasury Project (Sarajedini et al. 2007). We also derived the global mass functions, structural parameters and dark remnant fractions of the studied clusters by modelling their observed mass functions, velocity dispersion profiles and surface density profiles with isotropic, multimass King–Michie models (Gunn & Griffin 1979; Sollima, Bellazzini & Lee 2012). Our results showed that the derived global mass functions could generally be well described by single power-law mass functions in the mass range 0.2 < m/M⊙ < 0.8 except for the least evolved clusters. We also found a tight anticorrelation between the present-day mass functions slope and the half-mass relaxation time of the clusters. In addition, we found that the mass fraction of dark remnants in a cluster correlates with the mass function slope of the cluster, in the sense that clusters with flatter mass functions have a higher remnant fraction.

In this paper, we investigate what the results obtained in Sollima & Baumgardt (2017) imply for the stellar-mass function with which globular clusters were born and for their subsequent evolution. To this end, we compare the observational data with a set of 16 N-body simulations of star clusters starting with different initial mass functions (IMFs), particle numbers, half-mass radii, orbits in their parent galaxy and black hole (BH) retention fractions. In addition, we also use data from the large grid of 900 N-body simulations recently published by Baumgardt (2017). Our paper is organized as follows. In Section 2, we describe our N-body simulations in greater detail. In Section 3, we compare the mass functions of the simulated clusters with the observed mass functions of Galactic globular clusters and in Section 4, we draw our conclusions.

* E-mail: h.baumgardt@uq.edu.au

© 2017 The Authors
Published by Oxford University Press on behalf of the Royal Astronomical Society
2 DESCRIPTION OF THE N-BODY RUNS

The simulations in this paper were made using the GPU-enabled version of the collisional N-body code NBODY6 (Aarseth 1999; Nitadori & Aarseth 2012). Clusters started with particle numbers between \(N = 65,536\) and 200,000 stars. The IMFs of the clusters were given by either Kroupa (2001), Chabrier (2003) or Salpeter (1955) mass functions. In all simulations, stars were distributed between mass limits 0.1 < \(m < 100\) \(M_\odot\) and stellar evolution was modelled by the stellar evolution routines of Hurley, Pols & Tout (2000), assuming a metallicity of \([\text{Fe}/\text{H}] = -1.30\). This metallicity is close to the average metallicity of Galactic globular clusters. We assumed a retention fraction of neutron stars of 10 per cent in our simulations. Neutron stars not retained in the simulation were given large enough kick velocities upon formation so that they leave the clusters. In most simulations, we also assumed a retention fraction of 10 per cent for the BHs; however, we also made simulations of star clusters with either 30 per cent, 50 per cent or 100 per cent BH retention fractions to test the influence of the BH retention fraction on the cluster evolution. The initial half-mass radii of the clusters were equal to either \(r_h = 1\), 2 or 4 pc to simulate the evolution of star clusters starting with different initial relaxation times. All clusters followed King (1966) density profiles initially with a dimensionless central potential \(W_0 = 5.0\).

The simulated clusters were moving on circular orbits through an external galaxy that was modelled as an isothermal sphere with constant rotational velocity of \(V_\odot = 220\) km s\(^{-1}\). The distances of the clusters from the centres were chosen such that most clusters had lifetimes between 13 and 30 Gyr so that they are dynamically evolved to various degrees when they reach globular cluster ages. This resulted in initial Galactocentric distances between 3.5 and 8.5 kpc. Most clusters did not contain primordial binaries; however, we also made one simulation of a star cluster starting with a primordial binary fraction of 10 per cent to see how binaries influence our results. The binary stars in this cluster were set up as described in Lützgendorf, Baumgardt & Kruithof (2013), with a flat period distribution between 1 and 10\(^6\) d and a thermal eccentricity distribution.

In addition to the N-body runs described above, we also used the best-fitting N-body models of individual globular clusters derived from the simulations of Baumgardt (2017). These models are based on N-body simulations of isolated star clusters starting with \(N = 100,000\) stars initially, which are scaled in mass and radius to match the velocity dispersion and surface density profiles of Galactic globular clusters. The stars in these simulations followed a Kroupa (2001) IMF between mass limits \(0.1 < m < 100\) \(M_\odot\) and a 10 per cent retention fraction was applied to all neutron stars and BHs formed in the simulations. In this paper, we only use the no-IMBH models of Baumgardt (2017).

Table 1 presents an overview of the performed N-body simulations. It gives for each simulation the number of cluster stars, the chosen IMF, the Galactic tidal radius, the initial relaxation time and lifetime of the cluster (defined by the time a cluster has lost 99 per cent of its initial mass), and the best-fitting power-law slopes \(\alpha\) of the global and central mass functions at \(T = 12\) Gyr.

3 RESULTS

3.1 Initial mass function

We first compare the global cluster mass functions determined by Sollima & Baumgardt (2017) with the evolution of clusters starting with different IMFs in order to determine the IMF of Galactic globular clusters. For star clusters evolving in a tidal field, the shape of the global mass function changes as a result of the preferential loss of low-mass stars due to mass segregation and the removal of outer cluster stars (Vesperini & Heggie 1997; Baumgardt & Makino 2003). If the cluster mass function is described by a power law \(N(m) \sim m^{-\alpha}\), the preferential loss of low-mass stars leads to an increase of the slope \(\alpha\).

\begin{table}[ht]
\centering
\begin{tabular}{lcccccccc}
\hline
Model & \(N\) & Mass function & \(R_\odot\) & \(M_\odot\) & \(r_h\) & BH ret. & \(r_t\) & \(t_{\text{Diss}}\) & \(\alpha_g\) & \(\alpha_i\) \\
Nr. & & (pc) & (M_\odot) & (pc) & (pc) & (Myr) & (Myr) & & \\
\hline
1 & 65,536 & Kroupa & 8500 & 40,815 & 2.0 & 0 & 10 & 50.79 & 219.0 & 20,520 & -0.52 \pm 0.01 & 0.13 \pm 0.02 \\
2 & 65,536 & Chabrier & 8500 & 42,710 & 2.0 & 0 & 10 & 51.56 & 206.8 & 20,110 & -0.50 \pm 1.02 & 0.26 \pm 0.03 \\
3 & 65,536 & Salpeter & 8500 & 25,021 & 2.0 & 0 & 10 & 43.14 & 353.1 & 16,450 & -0.63 \pm 0.02 & 0.37 \pm 0.04 \\
4 & 131,072 & Kroupa & 5000 & 83,853 & 2.0 & 0 & 10 & 45.33 & 282.2 & 20,750 & -0.56 \pm 0.01 & 0.09 \pm 0.03 \\
5 & 131,072 & Chabrier & 5000 & 89,355 & 2.0 & 0 & 10 & 46.30 & 270.1 & 20,540 & -0.91 \pm 0.01 & 0.15 \pm 0.03 \\
6 & 131,072 & Salpeter & 5000 & 49,569 & 2.0 & 0 & 10 & 38.04 & 364.5 & 16,510 & -0.85 \pm 0.01 & 0.30 \pm 0.04 \\
7 & 131,072 & Kroupa & 3500 & 83,853 & 2.0 & 0 & 10 & 32.24 & 282.2 & 13,420 & 0.51 \pm 0.02 & 1.35 \pm 0.04 \\
8 & 131,072 & Kroupa & 8500 & 83,438 & 1.0 & 0 & 10 & 64.57 & 100.9 & 30,020 & -1.02 \pm 0.01 & -0.30 \pm 0.03 \\
9 & 131,072 & Kroupa & 8500 & 82,777 & 1.0 & 0 & 10 & 64.41 & 112.0 & 29,525 & -0.99 \pm 0.01 & -0.36 \pm 0.01 \\
10 & 200,000 & Kroupa & 3500 & 127,642 & 2.0 & 0 & 10 & 37.09 & 336.6 & 17,950 & -0.41 \pm 0.01 & 0.43 \pm 0.03 \\
11 & 200,000 & Kroupa & 5000 & 127,523 & 4.0 & 0 & 10 & 52.14 & 937.9 & 31,240 & -0.78 \pm 0.01 & -0.47 \pm 0.02 \\
12 & 131,072 & Kroupa & 5000 & 83,281 & 2.0 & 0 & 30 & 45.24 & 276.9 & 21,750 & -1.16 \pm 0.01 & -0.36 \pm 0.01 \\
13 & 131,072 & Kroupa & 5000 & 83,281 & 2.0 & 0 & 50 & 45.24 & 276.9 & 22,850 & -1.16 \pm 0.01 & -0.36 \pm 0.01 \\
14 & 131,072 & Kroupa & 5000 & 83,281 & 2.0 & 0 & 100 & 45.33 & 281.5 & 14,450 & -1.07 \pm 0.01 & -1.16 \pm 0.01 \\
15 & 131,072 & Kroupa & 8500 & 83,755 & 1.0 & 0 & 50 & 45.29 & 101.0 & 32,400 & -1.13 \pm 0.01 & -0.45 \pm 0.03 \\
16 & 131,072 & Kroupa & 8500 & 83,438 & 1.0 & 0 & 100 & 64.57 & 101.0 & 33,150 & -1.18 \pm 0.01 & -0.69 \pm 0.01 \\
\hline
\end{tabular}
\end{table}

\footnotesize
\begin{itemize}
\setlength\itemsep{0em}
\item[1] In the following, we will therefore speak of globular clusters with more negative values of \(\alpha\) as being dynamically less evolved than clusters with larger values of \(\alpha\).
\end{itemize}
the observed mass functions. We have split the cluster sample of Sollima & Baumgardt (2017) into six different groups depending on the best-fitting power-law slope $\alpha_G$ of the global mass functions and show the average number of stars over all clusters in each group with solid circles. The mass functions of globular clusters flatten due to the preferential loss of low-mass stars, from mass functions strongly increasing towards low-mass stars in the lower left-hand panel to flat mass functions in the upper right-hand panel. In addition, the stellar-mass function of the clusters in the three left-hand panels also show a flattening towards low-mass stars. Fitting a power law only to the low-mass stars with $m < 0.40$ in the lower left-hand panel, for example gives a best-fitting slope $\alpha \approx -1$, while the higher mass stars with $m > 0.40$ are best fitted by $\alpha \approx -1.4$.

The solid lines in Fig. 1 depict the stellar-mass distribution of clusters 4–6 from Table 1. The cluster starting with a Kroupa mass function is shown by blue lines, while the clusters with Chabrier and Salpeter IMFs are shown by red and green lines, respectively. All depicted clusters started with $N = 131 072$ stars and had circular orbits at a Galactocentric distance of 5 kpc. For each cluster, we calculate the global mass function slope $\alpha_G$ for each snapshot during the evolution and split the snapshots into the same six groups as the globular clusters. It can be seen that the stellar-mass distribution in star clusters which start with either a Kroupa or Chabrier IMF is in very good agreement with the observed stellar-mass distribution of globular clusters in each panel. In contrast, the cluster that starts with a (single power law) Salpeter IMF overpredicts the number of low-mass stars with $\log m < -0.6$ and underpredicts the number of stars with $\log m \approx -0.4$. These deviations are present for the least evolved clusters in the lower left-hand panel and are also present for the more evolved clusters. We obtain similar results for models 1–3 that start with $N = 65 536$ stars, as well as for clusters that start with a Kroupa IMF and $N = 200 000$ stars and take this as strong evidence that the mass function of globular clusters was not a single power law at the low-mass end, but had a steeper slope for high-mass stars than for lower mass stars, with a break or turnover at around $m \approx 0.4 M_\odot$, in good agreement with what is expected for either a Kroupa or Chabrier IMF.

In order to further explore the initial distribution of cluster stars, we depict in Fig. 2 the observed mass function slope as a function of distance from the cluster centre for the six least evolved clusters from Sollima & Baumgardt (2017), excluding NGC 6304 where the mass function is probably influenced by background contamination, see discussion in Sollima & Baumgardt (2017), and NGC 5024 where the mass function cannot be reliably determined at the centre due to incompleteness). We concentrate on the least evolved clusters since in the dynamically more evolved clusters the initial stellar distribution has been strongly modified by the cluster evolution and ongoing dissolution and cannot be easily compared with the simulations of Baumgardt (2017). The observed mass functions are shown by red filled circles and lines in Fig. 2. It can be seen that all depicted clusters are mass segregated to various degrees since the mass function slopes decrease towards larger radii, implying a larger fraction of low-mass stars at larger radii. Also shown are the mass function slopes of the best-fitting $N$-body models from Baumgardt (2017) over the same radial range for each cluster. The clusters in the simulations by Baumgardt (2017) are isolated clusters, hence the global mass functions in these clusters do not evolve with time, unlike the mass functions in the observed clusters which change due to the preferential loss of low-mass stars. In order to account for this preferential loss of low-mass stars, we shift the mass function slopes of each $N$-body model up until we obtain the best fit to the observed mass function slope for each cluster. Except for this offset in the mass function (MF) slope $\alpha$, the radial variation of the mass function is the same in the theoretical models and the observed clusters. Since the clusters in the $N$-body simulations started unsegregated, the six depicted clusters must have also started without primordial mass segregation and the radial variation of the mass function seen in each cluster is only due to energy equipartition driven by two-body relaxation. Given the good agreement for the six depicted clusters, which span a large range of cluster masses and sizes, we conclude that most Galactic globular clusters started unsegregated. The only exception could be low-mass and low-density halo clusters like Pal 4, which are highly mass segregated despite having long relaxation times and for which $N$-body simulations have shown that the amount of mass segregation seen cannot be explained by dynamical evolution (Zonoozi et al. 2014, 2017).

3.2 Constraints on the cluster evolution

Sollima & Baumgardt (2017) found a tight anticorrelation between the half-mass relaxation time of globular clusters and their global mass function slopes. Fig. 3 compares the location of the Galactic globular clusters in the relaxation time versus mass function slope plane that they found with results of three $N$-body simulations that start with a Kroupa (2001) IMF. Half-mass relaxation times $t_{\text{h}}$ for the clusters in the $N$-body simulations were calculated from equations 2–62 of Spitzer (1987) using all stars still bound to the clusters...
The mass function of 35 Galactic GCs

Figure 2. Mass function slopes in projection as a function of distance from the cluster centre for the six least evolved clusters from Sollima & Baumgardt (2017). Red, solid lines and circles show the observed MF slopes, blue solid lines and triangles show the best-fitting $N$-body models from Baumgardt (2017) for each cluster. Dashed lines show the MF slopes from the $N$-body simulations shifted to correct for mass-loss. The variation of the mass function slope with radius seen in the globular clusters can be entirely explained by two-body relaxation, indicating that the clusters started without primordial mass segregation.

Figure 3. Global mass function slopes as a function of relaxation time for observed globular clusters (red circles) and three large $N$-body simulations of dissolving star clusters. Solid lines show the relaxation times of the simulated clusters, dashed lines show the simulated clusters after their relaxation times were multiplied by a factor 5 to account for the fact that Galactic globular clusters are more massive and more extended than the clusters studied in the $N$-body simulations. After scaling there is a good overlap between both, indicating that Galactic globular clusters are tidally limited.

at any given time. We show the evolution of three $N$-body simulations starting with different particle numbers, half-mass radii and Galactocentric distances but all having a low retention fraction of BHs. The evolution of the clusters in the simulations can be divided into two phases, in the initial phase the clusters expand due to stellar evolution mass-loss and also heating due to binary stars in the core until they fill their Roche lobes. In this phase, the relaxation times increase but there is no strong evolution in the global mass function since the clusters are not yet mass segregated, so clusters move to the right in the relaxation time versus global MF slope plane. In the second phase, the clusters have become mass segregated and their mass functions become depleted in low-mass stars due to mass-loss, so the MF slopes evolve towards more positive values. This two stage behaviour in the mass function evolution of star clusters was also found by Lamers, Baumgardt & Gieles (2013) and Webb & Vesperini (2016). At the same time, the clusters lose mass and shrink due to mass-loss and a decreasing tidal radius, hence their relaxation times decrease as well. As a result, the simulated clusters move from the lower right corner to the upper left in the relaxation time versus global MF slope plane.

Since the clusters in the $N$-body simulations are about a factor 10 less massive and also on average about 30 percent more compact than observed globular clusters by the time they are 12 Gyr old, we increase the relaxation times of the star clusters in the $N$-body simulations by a factor 5 to match the relaxation times of globular clusters and show these scaled curves by dashed lines in Fig. 3. The scaled $N$-body clusters will probably not correctly capture the initial phases of cluster evolution, in particular the time-scale for mass segregation and cluster expansion, but should describe the
evolution of star clusters once they have become mass segregated and fill their Roche lobes since then the evolution is driven mainly by a single process: mass-loss. It can be seen that the location of the observed globular clusters agrees very well with that of the clusters in the N-body simulations when corrected for the differences in the relaxation times, indicating that the anticorrelation between mass function slope and relaxation time found by Sollima & Baumgardt (2017) could be due to the ongoing dissolution of globular clusters. If correct, Fig. 3 also implies that most globular clusters studied by Sollima & Baumgardt (2017) are tidally filling and their sizes start to shrink as they lose more and more of their stars. Such an evolution seems reasonable for many of the depicted clusters. A globular cluster with a mass of $M = 3 \times 10^5 M_\odot$ orbiting at a distance of 4 kpc from the Galactic Centre, for example would have a Jacobi radius of $r_J = 60$ pc, and, assuming that $r_\odot/r_J \approx 0.10$ in the tidally filling phase (Küpper, Kroupa & Baumgardt 2008) would have a half-mass radius of $r_{\text{h}} = 6$ pc when tidally filling. Our simulated clusters moving at $R_\odot = 8.5$ kpc reach similar half-mass radii within a few Gyr, meaning that many globular clusters, especially those in the inner parts of the Milky Way should also become tidally filling within a Hubble time. In addition, using the formula for globular cluster lifetimes derived by Baumgardt & Makino (2003), we would expect the globular cluster described above to have undergone a significant amount of mass-loss within 12 Gyr and have experienced significant changes to its IMF, similar to the observed globular clusters.

Figs 4 and 5 depict the location of the Galactic globular clusters in a global MF slope versus inner MF slope plane. Inner mass function slopes are derived from all stars located between projected radii of $0.15 \, r_{\text{h}} \leq r \leq 0.25 \, r_{\text{h}}$, where $r_{\text{h}}$ is the projected half-light radius of a cluster. This radial range was chosen since in most clusters this is the innermost region where the completeness fraction is still higher than 80 per cent even for the faintest stars in the HST/ACS images. For comparison, we also depict the evolution of the mass function slope for several N-body simulations. In Fig. 4, we show simulations with a 10 per cent retention fraction of stellar-mass BHs, while in Fig. 5 we depict clusters with higher retention fractions. The evolution of the clusters in the N-body simulations also falls into two phases. The clusters start with global and inner MF slopes around $\alpha_g = \alpha_i \approx -1.5$ since they start from Kroupa IMFs without primordial mass segregation. Before core collapse, clusters are not strongly mass segregated, therefore the global mass function changes only slowly, while the inner mass function evolves rapidly as the clusters become mass segregated. This near constancy of the global mass function before core collapse was also found by Lamers et al. (2013) in N-body simulations. After core collapse, there is a strong evolution in both the inner and global mass function slope. Depending on the initial relaxation time of the clusters, core collapse happens at slightly different points in the global versus inner MF plane. Clusters with an initial relaxation time of $T_{\text{RH0}} = 100$ Myr are already mass segregated before any mass-loss has set in, while in clusters with $T_{\text{RH0}} = 900$ Myr core collapse takes nearly as long as the dissolution of the clusters. Both curves seem incompatible with the location of the observed globular clusters. The best agreement with the location of observed globular clusters is achieved for an initial relaxation time of $T_{\text{RH0}} \approx 300$ Myr, implying an initial half-mass radius of $r_\odot = 1$ pc for an $M_C = 3 \times 10^5 M_\odot$ cluster. Addition of 10 per cent primordial binaries leads only to a small change in the cluster evolution when all other parameters are kept the same (see the evolution of model 8 versus model 9).

The mass function slopes of globular clusters also fall into two phases similar to the N-body clusters: a strong evolution in the inner MF slope together with a near constant global MF slope until $\alpha_i$,
by the blue dash–dotted line and the shaded area in Fig. 6. The α−slope. In the latter phase, the difference between inner and global 0, followed by a rapid evolution in both inner and global MF area. Clusters in the N body simulations have a global MF slope of N−1.1 only after nearly all BHs have been removed from the clusters.

≈ 0, followed by a rapid evolution in both inner and global MF slope. In the latter phase, the difference between inner and global MF slope is nearly constant at α − α ≈ 1.1 as clusters evolve towards dissolution. Given the agreement between simulations and observations, we conclude that globular cluster mass functions are shaped by the same interplay of mass segregation and dissolution as the clusters in the N-body simulations. If correct, Fig. 4 indicates that about 80 per cent of the clusters in the sample of Sollima & Baumgardt (2017) have already undergone core collapse or are at least close to core collapse. In addition, globular clusters must have undergone a significant amount of mass-loss, since clusters in the N-body simulations that have lost half of their initial cluster stars have a global MF slope of α = −1.0. Clusters in the simulations with α = −0.5, which is a typical slope for the observed globular clusters, have already lost 75 per cent of their stars. Judging from Fig. 4, the most evolved globular clusters should already have lost 90 per cent of their initial cluster stars, and, for a constant mass-loss rate, should therefore dissolve within the next 1–2 Gyr. These estimates agree with the mass-loss estimates obtained by Webb & Leigh (2015), who also concluded that globular clusters must have undergone a strong mass-loss based on their present-day mass function slopes.

Fig. 5 shows the evolution of star clusters with high BH retention fractions of 30–100 per cent. Due to the high fraction of stellar-mass BHs, mass segregation is strongly suppressed in these clusters and none of them shows strong mass segregation for most of its evolution. This is also depicted in Fig. 6, which compares the difference between the global and the inner mass function slope for our N-body simulations with the observed differences for Galactic globular clusters. Galactic globular clusters have an average α ∼ −1.13 ± 0.32. The average α ∼ 1σ deviation are shown by the blue dash–dotted line and the shaded area in Fig. 6. The different curves in Fig. 6 show the evolution of the difference of α − α for six of the N = 131 072 and 200 000 star simulations from Table 1 that start with a Kroupa IMF. In most models, a decrease in the number of BHs is accompanied by an increase in the amount of mass segregation. Regardless of the assumed initial retention fraction of BHs, the observed amount of mass segregation can only be reached when the fraction of BHs still retained in the clusters N/ is only a few per cent of the fraction of all BHs that formed in the clusters. This poses a problem for the models that start with high initial retention fractions of either 50 per cent or 100 per cent. The only models that can reach large enough values α ∼ α are those that start with small initial relaxation times of T ∼ 100 Myr (e.g. model 16) and even in this model the BHs are exhausted very close to the end of the lifetime of the cluster. For larger initial relaxation times, the clusters dissolve before all BHs are ejected, hence mass segregation is either too slow (model 12) or no mass segregation is happening at all (model 14). We conclude that the current number of BHs in globular clusters must be rather small, if clusters formed with a Kroupa IMF then at most a few per cent of the initially formed BHs still remain in the clusters. For a typical globular cluster forming with M = 3 × 10^5 M⊙, this implies that no more than 50 stellar-mass BHs currently reside in the cluster.

Given their masses, globular clusters probably started with relaxation times of several hundred Myr, more similar to our clusters starting with r = 2 or 4 pc initial half-mass radius than the r = 1 pc clusters. In addition, as we have seen before, most globular clusters have probably already lost a sizeable fraction of their initial cluster mass, meaning that their lifetimes are of the order of 20 Gyr. A quick cluster dissolution together with the long initial relaxation times and the small current BH fraction is incompatible with a large initial BH retention fraction. We therefore conclude that the initial BH retention fraction in globular clusters was at most 50 per cent, otherwise it is impossible to explain the large amount of mass segregation seen in the clusters today.

4 DISCUSSION

We have compared the observed stellar-mass functions of 35 Galactic globular clusters recently determined by Sollima & Baumgardt (2017) from HST/ACS data with a set of large N-body simulations of star clusters dissolving in external tidal fields. We find that the observed mass functions are compatible with globular clusters having started from either Kroupa (2001) or Chabrier (2003) mass functions but are incompatible with Salpeter (1955) mass functions at the low-mass end. Despite a difference of up to 10^3 in cluster mass, the IMF of globular clusters is therefore almost the same as that seen for stars in open clusters and field stars in the Milky Way (Bastian, Covey & Meyer 2010). This is in agreement with theoretical star formation simulations that predict only a weak dependence of the shape of the stellar-mass function with environment (Myers et al. 2011; Hennebelle 2012). The amount of mass segregation seen in the least evolved globular clusters can be completely explained by two-body relaxation driven mass segregation. It therefore seems likely that globular clusters formed without primordial mass segregation at least among the low-mass stars with m < 0.8 M⊙.

The observations of Sollima & Baumgardt (2017) have shown that the average global mass function slope of globular clusters for stars with masses in the range 0.2 < m/M⊙ < 0.8 is around α = −0.5, higher by 1 than the slope of the best-fitting power-law MF for a Kroupa mass function slope over the same mass range. According to our simulations, clusters that have global mass
Peuten et al. (2016) showed that the absence of mass segregation in globular clusters with a low initial BH retention fraction of 10 per cent. Recently, we also estimate that a typical globular cluster should have lost about 75 per cent of its initial stars and about 2/3 of its initial mass since formation. If globular clusters underwent an even more dramatic mass-loss, as some scenarios used to explain the large fraction of second-generation stars in globular clusters imply (e.g. D’Antona & Caloi 2008; D’Ercole et al. 2008), then this mass-loss must have happened early on before globular clusters were significantly mass segregated.

We also find a strong amount of mass segregation within globular clusters, the average difference between the global mass function slope to the inner mass function slope (which we define as the mass function slope of stars around 20 per cent of the projected half-light radius) is about $\alpha_i - \alpha_g = -1.1$. Our simulations show that due to the effective suppression of mass segregation by stellar-mass BHs, such a large amount of mass segregation is only possible if the number of stellar-mass BHs currently residing in the clusters is only a few per cent of the initial number of BHs formed (for a Kroupa IMF). A decrease in the amount of mass segregation or complete suppression of mass segregation due to stellar-mass BHs has also been found previously by Webb & Vesperini (2016) and Alessandri et al. (2016). Our simulations show that clusters with BH retention fractions equal to or higher than 50 per cent are not able to reach the low required BH numbers before final cluster dissolution unless their initial relaxation times would have been of the order of 100 Myr or less. Such small relaxation times seem difficult to achieve for star clusters starting with several $10^5 M_\odot$.

We therefore conclude that the initial stellar-mass BH retention fractions were 50 per cent or less. This result is in agreement with Sippel & Hurley (2013), who found that the current number of BHs observed to be in binary systems with a main-sequence companion as well as the estimated total number of BHs in M22 can be matched with a low initial BH retention fraction of 10 per cent. Recently, Peuten et al. (2016) showed that the absence of mass segregation in NGC 6101 found by Dalessandro et al. (2015) can only be explained by a high stellar-mass BH retention fraction. However, as Fig. 2 shows, the HST/ACS data actually shows NGC 6101 to be mass segregated, hence the simulations by Peuten et al. (2016) also argue against a high BH retention fraction in NGC 6101.

The clusters studied here only contain up to 200,000 stars initially and even though we do not find significant differences between the clusters with different initial particle numbers studied here, it is not clear how our results scale to globular clusters that typically formed with a 5–10 times larger number of stars. For globular clusters in the inner parts of the Milky Way, where the tidal field is strong, it seems possible that they could have expanded from small initial sizes to become tidally filling within a few Gyr and then undergo significant mass-loss, e.g. undergo a similar evolution as the clusters in our simulations. Problems could arise for clusters in the outer parts of the Milky Way, where the tidal field is too weak to allow expansion up to the tidal radius and significant mass-loss (Zonoozi et al. 2011). For such clusters, additional mass-loss mechanisms, due to e.g. formation and evolution in a dwarf galaxy (Webb et al. 2017) or highly elliptic orbits (Zonoozi et al. 2017) might be necessary to create sufficient mass-loss to explain their present-day mass functions. Alternatively, we cannot completely rule out variations in the global mass functions or primordial mass segregation in some globular clusters. Simulations of individual globular clusters on their exact orbits through the Milky Way would help to further constrain their starting conditions, but are challenging since only low-mass or very extended globular clusters can be simulated with direct N-body simulations at the moment (Zonoozi et al. 2011; Heggie 2014; Wang et al. 2016), while Monte Carlo codes can currently only handle constant tidal field strengths.

ACKNOWLEDGEMENTS

We thank Elham Hasani Zonoozi and an anonymous referee for comments that helped improve the paper.

REFERENCES

Aarseth S. J., 1999, PASP, 111, 1333
Alessandrini E., Lanzoni B., Ferraro F. R., Micocchi P., Vesperini E., 2016, ApJ, 833, 252
Bastian N., Covey K. R., Meyer M. R., 2010, ARA&A, 48, 339
Baumgardt H., 2017, MNRAS, 464, 2174
Baumgardt H., Makino J., 2003, MNRAS, 340, 227
Chabrier G., 2003, PASP, 115, 763
D’Antona F., Caloi V., 2008, MNRAS, 390, 693
D’Ercole A., Vesperini E., D’Antona F., McMillan S. L. W., Recchi S., 2008, MNRAS, 391, 825
Dalessandro E., Ferraro F. R., Massari D., Lanzoni B., Micocchi P., Beccari G., 2015, ApJ, 810, 40
Gunn J. E., Griffin R. F., 1979, AJ, 84, 752
Heggie D. C., 2014, MNRAS, 445, 3435
Hennebelle P., 2012, A&A, 545, A147
Hurley J. R., Pols O. R., Tout C. A., 2000, MNRAS, 315, 543
King I. R., 1966, AJ, 71, 64
Kroupa P., 2001, MNRAS, 322, 231
Küpper A. H. W., Kroupa P., Baumgardt H., 2008, MNRAS, 389, 889
Lamers H. J. G. L. M., Baumgardt H., Gieles M., 2013, MNRAS, 433, 1378
Lüttgendorf N., Baumgardt H., Kroupa P., 2013, A&A, 558, A117
Myers A. T., Krumholz M. R., Klein R. I., McKee C. F., 2011, ApJ, 735, 49
Nittrodi K., Aarseth S. J., 2012, MNRAS, 424, 545
Peuten M., Zocchi A., Gieles M., Gualandris A., Hénault-Brunet V., 2016, MNRAS, 462, 2333
Salpeter E. E., 1955, ApJ, 121, 161
Sarajedini A. et al., 2007, AJ, 133, 1658
Sippel A. C., Hurley J. R., 2013, MNRAS, 430, L30
Sollima A., Baumgardt H., 2017, MNRAS, 471, 3668
Sollima A., Bellazzini M., Lee J.-W., 2012, ApJ, 755, 156
Spitzer L., 1987, Dynamical Evolution of Globular Clusters. Princeton Univ. Press, Princeton, NJ
Vesperini E., Heggie D. C., 1997, MNRAS, 289, 898
Wang L. et al., 2016, MNRAS, 458, 1450
Webb J. J., Leigh N. W. C., 2015, MNRAS, 453, 3278
Webb J. J., Vesperini E., 2016, MNRAS, 463, 2383
Webb J. J., Vesperini E., Dalessandro E., Beccari G., Ferraro F. R., Lanzoni B., 2017, MNRAS, 471, 3845
Zonoozi A. H., Küpær A. H. W., Baumgardt H., Haghi H., Kroupa P., Hilker M., 2011, MNRAS, 411, 1989
Zonoozi A. H., Haghi H., Küpær A. H. W., Baumgardt H., Frank M. J., Kroupa P., 2014, MNRAS, 440, 3172
Zonoozi A. H., Haghi H., Kroupa P., Küpær A. H. W., Baumgardt H., 2017, MNRAS, 467, 758

This paper has been typeset from a TeX/\LaTeX\ file prepared by the author.