Global Sensitivity Analysis for CERES-Rice Model under Different Cultivars and Specific-Stage Variations of Climate Parameters

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Abstract: Global sensitivity analysis (SA) has become an efficient way to identify the most influential parameters on model results. However, the effects of cultivar variation and specific-stage variations of climate conditions on model outputs still remain unclear. In this study, 30 indica hybrid rice cultivars were simulated in the CERES-Rice model; then the Sobol’ method was used to perform a global SA on 16 investigated parameters for three model outputs (anthesis day, maturity day, and yield). In addition, we also compared the differences in the sensitivity results under four specific-stage variations (vegetative phase, panicle-formation phase, ripening phase, and the whole growth season) of climate conditions. The results indicated that (1) parameter Tavg, G4, and P2O are the most influential parameters for all model outputs across cultivars during the whole growth season; (2) under the vegetative-phase variation of climate parameters; the variability of model outputs is mainly controlled by parameter P2O and Tavg; (3) under the panicle-formation-phase or ripening-phase variation of climate parameters, parameter P2O was the dominant variable for all model outputs; (4) parameter PORM had a considerable effect (the total sensitivity index, STi; STi > 0.05) on yield regardless of the various specific-stage variations of the climate parameters. Findings obtained from this study will contribute to understanding the comprehensive effects of crop parameters on model outputs under different cultivars and specific-stage variations of climate conditions.

Keywords: CERES-Rice; rice; cultivars; Sobol’ method; sensitivity analysis

1. Introduction

Process-based crop models play an important role in many applications such as crop management [1], yield prediction [2], climate change assessment [3], and improvements of crop genotypes [4]. These models simulate physiological and ecological processes of photosynthesis, respiration, and transpiration in detail during the crop growth season [5]. They have also been helpful in understanding the interactions between soil, crops, and the atmosphere [6]. However, these models have usually included a large number of parameters which are dynamic, nonlinear, and complicated [7,8]. Accordingly, these parameters could lead to more serious over-parameterization problems. Therefore, parameter identification has become an important and urgent problem in agro-biophysical prediction and model further application [8–10].

A sensitivity analysis (SA) is a prerequisite process in model parameter estimation. SA has been implemented to study the influence of individual parameters on the uncertainty of model outputs [11], and was used to identify the input parameters regarding impact significance on a model’s outputs [12,13]. After SA, the low-impact parameters were fixed as default values; and only high-impact parameters deserved to be costly calibrated [10,14,15]. Thus, SA was useful to improve model calibration efficiency by ignoring insensitive parameters [16]. SA methods have been categorized into local SA and global SA [17]. Local
SA has mainly calculated the influence of single parameter variability on model outputs by holding other variables or parameters at fixed values. It only analyzes the direct influence of parameters on the model results, while ignoring the indirect influence of the interactions between parameters on the model [9]. Local SA is easy to implement but could lead to unrealistic sensitivity results since the sensitivity of a specific parameter depends on the values of other parameters, which was particularly evident in the non-linear models [18]. In contrast, the global SA takes into account the influence of multiple parameters and their interactions on the model results, which was suitable for nonlinear models with more input parameters [8]. The commonly used global SA methods include the Morris method [19], Fourier amplitude test (FAST) method [20], Sobol’ method [21], and the extend FAST (EFAST) method [22]. Because global SA methods consider the interactions of parameters and nonlinear responses, they were desirable to explore the parameter sensitivity and uncertainty analysis of model outputs in mechanistic models such as the hydrologic models [23,24], climate models [25,26], and ecological models [27,28].

In recent years, global SA has been successfully applied to implement parameter identification and uncertainty analysis for crop growth models [18,29–32]. SA and uncertainty of crop models under the different ranges of parameter variations have been explored. For example, Tan et al. [33] used a regression-based method to carry out global SA on 16 parameters in the ORYZA model under different ranges of parameter perturbation; and the results indicated that ±30% perturbation was suggested in sensitivity and uncertainty analysis. The effects of parameter variation range on model outputs over time were also discussed by Jin et al. [16]. Besides the effects of parameter perturbation range on sensitivity, the effects of different environment and climate conditions on model sensitivity in crop models have been reported. Liu et al. [34] conducted global SA of the APSIM-Oryza rice model under different environment and CO₂ level conditions by using the EFAST method; they demonstrated that the orders of the same influential parameters in different climate conditions were different. Roberto et al. [31] also analyzed the parameter sensitivity to the rice model WARM under various environment and climatic conditions and then the necessity of SA within different modeling environments was emphasized.

Although a number of global SA studies have been performed for crop models [8,16,31], some limitations need to be further addressed: (i) Few studies have paid attention to the effects of crop genotype variations on SA. The SA results derived from one cultivar could not be directly transferable to another cultivar. (ii) A systematical description of the effects of specific-stage climate variations on SA results is still unclear.

Therefore, it is necessary to explore the responses of model outputs to input parameters or variables under different genotypes, and specific-stage climate variations. In this study, the Sobol’ method was used to implement global SA of the CERES-Rice model for thirty rice genotypes and four specific-stage climate variations. The specific objectives were to: (1) explore whether the sensitivity rankings of the investigated parameters among different cultivars were statistically different for the model outputs (anthesis day, ADAP; physiological maturity day, MDAP; and yield); (2) identify the most influential parameters for model results in the CERES-Rice model among different cultivars; (3) highlight the differences in effects of the input parameters on the crop model outputs under specific-stage variations of climate parameters.

2. Materials and Methods

2.1. Field Experiments

The experiment site was located at the Longping High-tech Rice Breeding Base (28°19’ N, 112°40’ E), Ningxiang District, Changsha City, Hunan Province, China. This area belongs to a subtropical monsoon climate, which is characterized by mild climate, abundant precipitation, simultaneous rain and heat, and four distinct seasons. The annual average temperature and rainfall are 16.8 °C and 1358 mm, respectively. The soil at the experimental site has a typical fine-loam profile from 0–20 cm. The detailed soil physical and chemical properties are shown in Table 1.
Table 1. Soil profile properties at the experimental site.

| Layer (m) | Clay (%) | Silt (%) | OC (%) | TN (%) | LL (%) | DUL (%) | SAT (%) | BD (g cm$^{-3}$) |
|-----------|----------|----------|--------|--------|--------|---------|---------|------------------|
| 0–0.2     | 25.96    | 28.6     | 2.13   | 0.18   | 21.4   | 37.0    | 48.3    | 1.26             |
| 0.2–0.4   | 25.13    | 27.1     | 2.12   | 0.20   | 20.9   | 36.2    | 48.0    | 1.27             |
| 0.4–0.6   | 23.03    | 25.7     | 1.73   | 0.17   | 18.8   | 32.7    | 46.4    | 1.32             |
| 0.6–0.8   | 22.99    | 27.9     | 1.51   | 0.19   | 18.2   | 32.0    | 46.2    | 1.33             |
| 0.8–1.0   | 24.5     | 28       | 1.58   | 0.16   | 19.2   | 33.2    | 46.5    | 1.32             |

Note: OC, organic carbon; TN, total nitrogen; LL, lower limit; DUL, drained upper limit; SAT, saturation; BD, bulk density.

Thirty indica hybrid rice cultivars were investigated at the experiment site in 2018. Among these cultivars, there were 12 mid-season rice cultivars, 9 late-season rice cultivars and 9 one-season-late rice cultivars. All cultivars were transplanted in a randomized complete block with 3 replicates. The planting density was 33 hills m$^{-2}$. Each cultivar had the same cultivated area with 2.5 m × 5.5 m. All the experimental cultivars had the same fertilizer treatment with 195 kg ha$^{-1}$ N, 112 kg ha$^{-1}$ P$_2$O$_5$ and 112 kg ha$^{-1}$ K$_2$O. Other field management practices followed the local standard procedures for rice production in this region.

2.2. Data Observation

The observations of the rice phenological stages were collected once every 1 to 3 days during the rice growth season. The data of critical phenological events such as sowing, transplanting, initial heading, anthesis, full heading, and maturity stages are listed in Table 2. The specific descriptions of these phenological stages were presented by Yang et al. [35] and Fageria [36]. At maturity, all the rice in each plot was harvested and hand-threshed. The collected grains were put into an oven at 75 °C until their weights had no change (about 72 h) and then weighed by an electronic balance (±0.1 g). Subsequently, the 1000-grain weight was measured by local agro-technicians in the laboratory.

Table 2. The observed phenology of the different rice cultivars in 2018 at the experiment station.

| Type of Cultivar   | Sowing   | Transplanting | Initial Heading | Flowering   | Full Heading | Maturity                   |
|--------------------|----------|---------------|-----------------|-------------|--------------|----------------------------|
| Mid-season         | 15 May   | 6 June        | 2 August–10 August | 4 August–12 August | 7 August–14 August | 10 September–16 September |
| Late-season        | 24 June  | 15 July       | 29 August–5 September | 31 August–7 September | 2 September–9 September | 17 October–24 October     |
| One-season-late    | 10 June  | 29 June       | 24 August–30 August | 26 August–1 September | 29 August–3 September | 10 October–12 October     |

2.3. CERES-Rice Model

2.3.1. Model Description

The CERES-Rice model was first developed by the American IBSNA scientists in the 1980s. This model has been integrated in the Decision Support System for the Agrotechnology Transfer (DSSAT) system. Combining with the relevant modules of the DSSAT system, the CERES-Rice model could analyze the effects of many factors on the growth and development of paddy rice. It mainly consists of three parts: (1) an input module including input files of weather, soil, field management, and species genetic characteristic parameters, as well as observed data, etc.; (2) an output and analysis module including all simulation results and output files of data analysis; (3) a physiological and ecological process simulation module. Thus, the CERES-Rice model can quantitatively describe the basic process of rice growth and development under different environmental conditions. At present, the CERES-Rice model has been widely applied in many applications such as yield estimation [37], climate change assessment [38], and field management [39].
2.3.2. Crop Modeling

To run the CERES-Rice model, parameters and inputs including weather data, soil profile information, field management data, and genotype parameter data were required. The minimum requirements of weather data contained daily minimum and maximum temperature, daily rainfall, and daily solar radiation. These data were collected from the local weather station. The soil profile data is listed in Table 1. Field management data are introduced in Section 2.1. In the CERES-Rice model, the genotype parameters included cultivar, species, and ecotype coefficients. There were eight cultivar coefficients which were used to describe the hereditary characteristics of the specific genotypes. Among them, four cultivar parameters (P1, P2R, P5, P2O) were related to phenology and another four parameters (G1, G2, G3 and G4) were pertinent to rice growth and development. The species coefficients were set as default values. At present, the ecotype coefficients are not available for common users in the CERES-Rice model. Accordingly, only eight cultivar parameters were determined in this study.

The time period (growing degree days, °C·d) from beginning of grain filling (3–4 days after flowering) to physiological maturity (P5) was calculated based on observation data. Single grain weight (G2) was set based on 1000-grain weight. The calculation of cultivar parameters based on observed data in DSSAT has been described by Yan et al. [40]. The specific calculation processes of P5 and G2 were as follows:

\[
P5 = \sum_{i=1}^{m} \left( \frac{Tavg_i - T_{base}}{Tavg_i - T_{base}} \right) \begin{cases} \frac{Tmax_i + Tmin_i}{2} & \text{if } Tavg_i \leq T_{base} \\ T_{upper} & \text{if } Tavg_i \geq T_{upper} \end{cases}
\]

\[
G2 = \frac{W}{1000}
\]

where \(i = 1, 2, \ldots, m\) days between beginning of grain filling and physiological maturity. On the \(i_{th}\) day, \(Tavg_i\) is the daily average temperature (°C); \(Tmin_i\) is the daily minimum temperature (°C); \(Tmax_i\) is the daily maximum temperature (°C); \(T_{base}\) is the base temperature of 9 °C; \(T_{upper}\) is set to 40 °C. In equation 2, \(W\) represents the 1000-grain weight (g).

Other six parameters (P1, P2R, P2O, G1, G3 and G4) of each rice cultivar were determined by the Generalized Likelihood Uncertainty Estimation (GLUE) method which has been widely used in model calibration [41,42]. The specific procedures of the GLUE method are mainly as follows [15,43]:

1. Set parameter range by using the default range (Table A1) in the CERES-Rice model. Uniform parameter distributions were assumed to generate parameter sets. In this study, 10,000 parameter sets were randomly generated by Python 3.6.
2. Select the observation data including anthesis date, maturity date, and grain yield as our objectives.
3. Run the CERES-Rice model. The executable file “DSCSM047.exe” was looped called Python 3.6 based on the abovementioned parameter sets.
4. Calculate the likelihood value. A likelihood function which was described by He et al. [41] was implemented to obtain likelihood values based on simulations and observations.
5. Calculate the cultivar parameters based on the maximum likelihood value.

2.4. Sensitivity Analysis

2.4.1. Sobol’ Method

In this study, the Sobol’ algorithm was implemented to rank sensitivity of input parameters or variables to the model outputs (ADAP, MDAP and yield). The Sobol’ global SA calculates the analysis of variance-based decomposition of output variance, where the main effects and interaction terms can be computed [44]. The Sobol’ sensitivity index is the fraction of total variance which is attributed to any individual factor or combination of factors [45]. In addition, the Sobol’ method can calculate the total sensitivity index (ST), defined as the sum of the first-order and higher-order effects involving all the input factors.
With \( m \) quantitative input factors, the decomposition of variance \( \text{var}(Y) \) can be calculated as follow:

\[
\text{var}(Y) = \sum_{i=1}^{m} v_i + \sum_{1 \leq i < j \leq m} v_{ij} + \cdots + v_{1,2,\ldots,m} \tag{3}
\]

where \( v_i \) is the variability based on the main effect of input factor \( x_i \); \( v_{ij} \) is the variability based on the interaction effect between input factors \( (x_i \text{ and } x_j) \); \( v_{1,2,\ldots,m} \) is the variability based on the interaction effect between all input factors \( (x_1, x_2, \ldots, x_m) \). \( \text{var}(Y) \) represents the variability of \( Y \) including the overall uncertainty of the input factors. The sensitivity indices are calculated from Equation (3) by dividing the individual importance measures by the total variance \( \text{var}(Y) \).

\[
S_i = \frac{v_i}{\text{var}(Y)} \tag{4}
\]

\[
SI_{ij} = \frac{v_{ij}}{\text{var}(Y)} \tag{5}
\]

where \( S_i \) is defined as the first order sensitivity index of input factor \( x_i \), representing the main effect of factor \( x_i \) on the output. \( SI_{ij} \) is defined as the second-order sensitivity index which represents the interaction effect of two factors \( x_i \) and \( x_j \).

Sobol’ input samples were generated by using the Python library “SALib” and executed by a size of \( m(2n + 2) \) model input sets in Python 3.6, where \( m \) required a range of 100 or larger [44]. Sixteen parameters \( (n) \) were selected to implement global SA (Table 3). In this study, we used \( m = 350 \) and \( n = 16 \) for a total of 11,900 input parameter sets for each cultivar. Four specific-stage variations of climate parameters were considered (Figure 1). The investigated stages include the whole growth season, vegetative phase, panicle-formation phase and ripening phase. Accordingly, the total number of model executions was \( 30 \times 11,900 \times 4 = 1,428,000 \). The majority of global SA computations described in this paper were performed on the High-Performance Computing System at the Institute of Soil Science, Chinese Academy of Sciences.

Table 3. Description of the 16 investigated parameters in the CERES-Rice model.

| Type        | Parameter | Description                                                                 | Unit   | Range  |
|-------------|-----------|-----------------------------------------------------------------------------|--------|--------|
| Cultivar    | P1        | Time period in °C above a base temperature of 9 °C during the basic vegetative phase. | GDD (°C) | ±30%   |
|             | P2O       | Critical photoperiod (in hours) at which the development occurs at a maximum rate. | hours  | ±30%   |
|             | P2R       | Extent to which phasic development leading to panicle initiation is delayed for each hour increase in photoperiod above P2O | GDD h\(^{-1}\) | ±30%   |
|             | P5        | Time period in °C above a base temperature of 9 °C from beginning of grain filling (3–4 days after anthesis) to physiological maturity. | GDD (°C) | ±30%   |
| Species     | G1        | Potential spikelet number coefficient. | –      | ±30%   |
|             | G2        | Single grain weight (g) under ideal growing conditions. | g      | ±30%   |
|             | G3        | Tillering coefficient relative to IR64 cultivar under ideal conditions. | –      | ±30%   |
|             | G4        | Temperature tolerance coefficient. | –      | ±30%   |
|             | SHFC      | Shock calculation method (1-standard, 2-Salaam) | –      | ±30%   |
|             | RWEP      | Species coefficient. | –      | ±30%   |
|             | PORM      | Minimum pore space. | –      | 0–0.3  |
|             | RWMX      | Max root water uptake. | –      | ±30%   |
|             | RLWR      | Root length weight ratio. | –      | ±30%   |
| Climate     | SRAD      | Daily solar radiation. | MJ m\(^{-2}\) day\(^{-1}\) | ±30%   |
| parameter   | Tavg      | Daily average temperature. | °C     | ±30%   |
|             | RAIN      | Daily rainfall. | mm day\(^{-1}\) | ±30%   |
Figure 1. Typical workflow for global SA across 30 cultivars in the CERES-Rice model. Strategy 1–4 represent the variations of climate parameters at vegetative phase, panicle-formation phase, ripening phase, and the whole growth season, respectively.

2.4.2. Top-Down Concordance Coefficient (TDCC)

The top-down concordance coefficient (TDCC) can quantify agreements among multiple rankings. The TDCC adopts the savage scoring method to emphasize the consistency of influential parameter rankings and to de-emphasize the inconsistency of non-influential parameter rankings [46]. The TDCC was calculated using the following equation:

\[ S_{ij} = \sum_{i=r_{ij}}^{n} \frac{1}{i} \]  

\[ TDCC = \frac{\sum_{i=1}^{m} \left( \sum_{j=1}^{n} S_{ij} \right)^2 - m^2n}{m^2 \left( n - \sum_{i=1}^{n} \frac{1}{i} \right)} \]  

where \( S_{ij} \) is the savage score of the \( i_{th} \) parameter in the \( j_{th} \) SA experiment; \( r_{ij} \) is the rank of the \( i_{th} \) parameter in the \( j_{th} \) SA experiment; \( n \) is the number of investigated parameters; and \( m \) is the number of SA objectives.

The \( p \)-value was calculated to test the TDCC’s significance, which is calculated as follows:

\[ T = m(n - 1)TDCC \]  

where \( T \) is close to the chi-squared distribution with \( n - 1 \) degrees of freedom. In general, rankings were considered statistically consistent if the \( p \)-value derived from TDCC was smaller than 0.05.
3. Results

3.1. Distribution of Observation Data across Different Cultivars

The distributions of observations including dates of anthesis and maturity, and grain yield are presented in Table 4. Among different cultivar types, the mid-season rice had the earliest date of anthesis. Although, the sowing date for late-season cultivars was two weeks later than that for one-season-late cultivars, the anthesis dates for these two cultivar types were close. The mean anthesis dates were 8 August, 3 September, and 29 August for mid-season, late-season, and one-season-late rice cultivar types, respectively in 2018. As for physiological maturity, all the mid-season rice cultivars were harvested in September, and all late-season and one-season-late rice cultivars were harvested in October. The mean maturity dates for mid-season, late-season, and one-late-season rice cultivars were 12 September, 20 October, and 11 October, respectively. Additionally, the yield of one-season-late cultivars tended to be slight larger than that of mid-season cultivars; the yield obtained from late-season cultivars was the lowest.

| Observation Index | Cultivar Type     | Number of Cultivars | Statistical Indicators |
|-------------------|-------------------|---------------------|------------------------|
|                   |                   |                     | Mean       | Median     | 25th Percentile | 75th Percentile |
| Anthesis date     | Mid-season        | 12                  | 8-August   | 8-August   | 7-August       | 9-August       |
|                   | Late-season       | 9                   | 3-September | 2-September | 1-September   | 4-September   |
|                   | One-season-late   | 9                   | 29-August  | 30-August  | 26-August     | 30-August     |
|                   | Mid-season        | 12                  | 12-September | 13-September | 10-September | 14-September |
| Maturity date     | Late-season       | 9                   | 20-October | 19-October | 18-October    | 21-October    |
|                   | One-season-late   | 9                   | 11-October | 12-October | 11-October    | 12-October    |
|                   | Mid-season        | 12                  | 9.7        | 9.6        | 9.4           | 10.1          |
| Yield (t ha$^{-1}$) | Late-season       | 9                   | 8.2        | 7.8        | 8.0           | 8.5           |
|                   | One-season-late   | 9                   | 9.9        | 9.7        | 9.6           | 10.1          |

3.2. Sensitivity Analysis during the Rice Growth Season

For both ADAP and MDAP, parameters P2O, G4, Tavg were more influential than other parameters among different cultivar types (Figure 2). G4 in late-season and mid-season cultivars showed larger inter-cultivar variability than that in one-season-late cultivars. Tavg had the largest influence on $ST_i$ values for phenology in all cultivars. For yield, parameters Tavg and P2O had a markedly larger influence and inter-cultivar variability. The variations of $ST_i$ values were similar in different cultivar types. In general, the more influential parameters (Tavg and P2O) showed a more evident difference between cultivars.

Figure 3 shows the mean $S_i$ values and interactions between parameters under different cultivar types when the variation of climate parameters occurred for the whole growth season. Different cultivar types demonstrated similar effects on the sensitivity results of the investigated parameters for ADAP, MDAP, and yield; for instance, the most influential parameters (Tavg, P2O, G4) were the same. It is worth mentioning that the influence of the interaction among parameters on all outputs of the CERES-Rice model was notable. For ADAP, the interaction indices of Tavg, P2O, and G4 contributed to 64.9–90.7%, 56.1–77.4%, and 73.5–86.6%, respectively in late-season, one-season-late, and mid-season cultivar types. For MDAP, though the most influential parameters were the same as those for ADAP, the interaction effects of these parameters were slightly smaller and contributed to 51.2–81.7%, 43.0–70.2%, and 51.9–81.5%, respectively in late-season, one-season-late, and mid-season cultivar types. For yield, the interaction effects of cultivar parameters contributed approximately 90% such as P1, P2R, P2O, and G4. The climate parameter Tavg contributed 54.8%, 62.5%, and 55.2% for the variance of yield, respectively in late-season, one-season-late, and mid-season cultivar types.
Figure 2. Distribution of Sobol’ total order effects ($ST_i$) for 16 investigated parameters under different cultivar types during the whole rice growth season: (a–c) outputs for ADAP, MDAP, and yield.

Figure 3. The mean first order index ($S_i$) and interactions under different cultivar types during the whole rice growth season. The bottom title of each subfigure means the SA for specific outputs (ADAP, MDAP, and yield) under different cultivar types.
Table 5 shows the values of TDCC under the different cultivar types. The different cultivars in the same cultivar type had no noticeable effect on the parameter ranking for the model outputs. The TDCC values were larger than 0.93 for all output variables. Additionally, the TDCC values in different cultivar types were greater than 0.98 for all output variables. The corresponding p-values are not presented in this study but were less than 0.05. In general, different cultivars had no statistical influence on the rankings of the sensitivity parameters.

Table 5. TDCC values based on the results of Sobol’ total order effects ($ST_i$) under the same cultivar type and different cultivar types over the whole growth season.

| Model Output | Same Cultivar Type | Different Cultivar Types |
|--------------|--------------------|-------------------------|
|              | Late-Season        | One-Season-Late          | Mid-Season | L-O | L-M | O-M |
| ADAP         | 0.95               | 0.98                    | 0.94       | 0.99 | 0.99 | 0.99 |
| MDAP         | 0.98               | 0.96                    | 0.98       | 0.98 | 0.98 | 0.98 |
| Yield        | 0.98               | 0.99                    | 0.97       | 1.00 | 1.00 | 1.00 |

Note: L-O rice represents the cultivars between late-season and one-season-late cultivar types; L-M rice represents the cultivars between late-season and mid-season cultivar types; O-M rice represents the cultivars between one-season-late and mid-season cultivar types.

3.3. Sensitivity Analysis under Specific-Stage Variations of Climate Parameters

3.3.1. Sensitivity Analysis under the Variation of Climate Parameters at the Vegetative Phase

Figure 4 illustrates the mean $S_i$ values and interactions between parameters under different cultivar types when the variation of climate parameters occurs at the vegetative phase. At this stage, the effects of $P2O$ ($S_i$ ranged from 0.61 to 0.70) and $Tavg$ ($S_i$ ranged from 0.12 to 0.25) on model outputs (ADAP and MDAP) were significant, while the interactions between parameters were non-significant. Except for $P2O$ and $Tavg$, the species parameter PORM showed a notable effect on yield ($ST_i > 0.05$). Different cultivar types indicated no differences in the sensitivity results of the investigated parameters for ADAP, MDAP, and Yield. Parameter $P2O$ was the most sensitive for all model outputs, whereas the growth-related parameters (e.g., $G1$, $G2$, $G3$, and $G4$) showed negligible effects on the model outputs ($ST_i < 0.05$). The sensitivity rankings of the 16 investigated parameters were statistically consistent among different cultivars (Table 6).

Table 6. TDCC values based on the results of Sobol’ total order effects ($ST_i$) under the same cultivar type and different cultivar types with variation of climate parameters at the vegetative phase.

| Model Output | Same Cultivar Type | Different Cultivar Types |
|--------------|--------------------|-------------------------|
|              | Late-Season        | One-Season-Late          | Mid-Season | L-O | L-M | O-M |
| ADAP         | 0.98               | 0.99                    | 0.98       | 1.00 | 1.00 | 1.00 |
| MDAP         | 0.98               | 0.97                    | 0.95       | 0.99 | 0.98 | 0.98 |
| Yield        | 0.96               | 0.97                    | 0.99       | 0.99 | 0.97 | 0.97 |

Note: L-O rice represents the cultivars between late-season and one-season-late cultivar types; L-M rice represents the cultivars between late-season and mid-season cultivar types; O-M rice represents the cultivars between one-season-late and mid-season cultivar types.
model outputs ($S_{T_0}$ < 0.05). The sensitivity rankings of the 16 investigated parameters were statistically consistent among different cultivars (Table 6).

Table 6. TDCC values based on the results of Sobol’ total order effects ($S_{T_0}$) under the same cultivar type and different cultivar types with variation of climate parameters at the vegetative phase.

| Model Output | Same Cultivar Type | Different Cultivar Types |
|--------------|--------------------|-------------------------|
|              | Late-Season        | One-Season-Late         | Mid-Season | L-O     | L-M     | O-M     |
| ADAP         | 0.99               | 0.99                    | 0.99       | 0.99    | 0.99    | 0.99    |
| MDAP         | 0.96               | 0.96                    | 0.97       | 0.96    | 0.96    | 0.96    |
| Yield        | 0.96               | 0.98                    | 0.97       | 0.98    | 0.98    | 0.98    |

Note: L-O rice represents the cultivars between late-season and one-season-late cultivar types; L-M rice represents the cultivars between late-season and mid-season cultivar types; O-M rice represents the cultivars between one-season-late and mid-season cultivar types.

3.3.2. Sensitivity Analysis under Variation of Climate Parameters at the Panicle-Formation Phase

Figure 5 presents the sensitivity indices of the 16 investigated parameters for model outputs simulated in late-season, one-season-late, and mid-season rice cultivar types, respectively under the panicle-formation-phase variation of climate parameters. At this stage, climate parameters (SRAD, Tavg, and RAIN) had no influence on the variations of all model outputs; the $S_{T_0}$ values were less than 0.05. For ADAP and MDAP, only phenology-related parameters (P1, P2R, P5, and P2O) had a notable influence on the model outputs. For yield, parameter P2O ($S_{T_0}$ > 0.70) was the most sensitive parameter, followed by PORM ($S_{T_0}$ > 0.10). The growth-related parameters (G1 and G2) indicated slight effects on yield. In general, the effects of single parameters ($S_i$) on model outputs were significant, while interactions between parameters were non-significant. In addition, the sensitivity rankings of parameters were statistically consistent among various cultivars (Table 7).

Table 7. TDCC values based on the results of Sobol’ total order effects ($S_{T_0}$ ) under the same cultivar type and different cultivar types with variation of climate parameters at the panicle-formation phase.

The mean first order index ($S_i$) and interactions under different cultivar types under variation of climate parameters at the vegetative phase. The bottom title of each subfigure shows the SA for specific outputs (ADAP, MDAP, and yield) under different cultivar types.
3.3.3. Sensitivity Analysis under Variation of Climate Parameters at the Ripening Phase

Figure 6 shows the mean sensitivity indices of the 16 investigated parameters under the ripening-phase variation of climate parameters, simulated on late-season, one-season-late, and mid-season rice cultivar types, respectively. For ADAP, the cultivar types showed no significant influence on the ranks of parameter sensitivities. Parameter P2O was the most influential parameter for ADAP ($S_{Ti} > 0.82$). Except for phenology-related parameters (P2, P2R and P2O), other parameters demonstrated no effect on the variation of ADAP ($S_{Ti} < 0.05$). For MDAP, parameter Tavg indicated more effects on MDAP in the late-season cultivar type than in the one-season cultivar type. However, Tavg in the mid-season cultivar type showed negligible effects on the variability of MDAP ($S_{Ti} < 0.05$). For yield, parameter P2O and PORM were the most sensitive parameters. The growth-related parameters (G1 and G2) had minor effects on yield. The effects of interactions between parameters on the model outputs were non-significant. Table 8 shows that the TDCC values among different rice cultivars were above 0.95.

**Table 7. TDCC values based on the results of Sobol’ total order effects ($ST_{i}$) under the same cultivar type and different cultivar types with variation of climate parameters at the panicle-formation phase.**

| Model Output | Same Cultivar Type                  | Different Cultivar Types |
|--------------|------------------------------------|-------------------------|
|              | Late-Season | One-Season-Late | Mid-Season | L-O | L-M | O-M |
| ADAP         | 0.99        | 1.00           | 0.99       | 0.99 | 0.99 | 0.99 |
| MDAP         | 0.96        | 0.97           | 0.97       | 0.96 | 0.95 | 0.95 |
| Yield        | 0.97        | 0.98           | 0.98       | 0.99 | 0.98 | 0.98 |

Note: L-O rice represents the cultivars between late-season and one-season-late cultivar types; L-M rice represents the cultivars between late-season and mid-season cultivar types; O-M rice represents the cultivars between one-season-late and mid-season cultivar types.
4. Discussion

4.1. Sensitivity Analysis of Different Cultivars for Model Outputs during the Rice Growth Season

Crop growth models become more complicated due to the improvements in the understanding of the physiological and ecological processes and their interactions and the increased computing power of the corresponding simulators with several related parameters to estimate. Global SA is an important component of modelling practices which could help in factor prioritization [47], and the Sobol’ method demonstrated the sensitivity of the CERES-Rice model with a variety of 16 investigated parameters among 30 rice cultivars for ADAP, MDAP, and yield during the rice growth season. Although, only one year of data was used to analyze the SA of the experiment area, it has been reported that data from one year or a single growth season can be used for the global SA [16,33]. Besides, the sensitivity ranking of the parameters was not significantly affected by the year [48]. The computationally expensive Sobol’ SA method helped us to understand the overall functioning of the CERES-Rice model in cultivar variations of the breeding trials and then to implement a quantitative evaluation of SA for the model outputs. Although, variance-based methods have expensive computation cost, they can explore all regions of input space and consider both interaction and nonlinear response [21,49].

For different cultivars, the TDCC values for all model outputs were more than 0.90 (Table 5); this indicated that the effects of cultivars on parameter rankings were not significant (p < 0.05), which is due to two reasons: (1) different cultivars in the breeding trials showed similar phenotypic traits (Table 4) and (2) these genotypes were all obtained from two parents in this study. In addition, the cultivar types (e.g., late-season, one-season-late, and mid-season types) had little effect on the ranking of the influential parameters for model outputs. However, due to the variation of growth duration length, the distribution of sensitivity index values of inter-cultivars was slightly inconsistent in the different cultivar types (Figure 2).

As for specifically influential parameters, the Tavg, G4, and P2O (ST, > 0.24) were the most sensitive parameters for the variation of ADAP and MDAP. In the CERES-Rice model, the development rate of rice depended on the degree days (DD). Parameter Tavg which determined the daily maximum and minimum temperature was a key factor in...
calculating the day’s value of DD [50]. Accordingly, parameter $T_{avg}$ ($ST_i > 0.61$) was the most influential parameter for rice phenology among all cultivars. Parameter G4 was the temperature tolerance coefficient, the influences of parameter interactions were greater than the influences of the first-order contribution (Figure 3). Parameter P2O represented the longest day length when the development rate was maximum. Compared to other phenology-related parameters (P1, P2R, and P5), parameter P2O was more sensitive to phenology, which was mainly because the longest day length in the breeding site was larger than P2O; thus, a notable effect on the results. For yield, the most sensitive parameters were similar to those for ADAP and MDAP (Figure 3), which could be explained by the close relationship between growth duration length and panicle formation. It was of note that the species parameter PORM (minimum pore space) had considerable influence on yield. All the $ST_i$ values of PORM among different cultivars were larger than 0.05.

4.2. Effects of Specific-Stage Variations of Climate Parameters on Sensitivity

This study demonstrated a new comprehensive insight into the SA of a crop model with variations of climate parameters at specific stages. The variation of climate parameters was divided into three phases: (1) vegetative phase (sowing to initial heading), (2) panicle-formation phase (initial heading to full heading), and (3) ripening phase (full heading to maturity). When the variation of climate parameters occurred at the vegetative phase, $T_{avg}$ showed significant effects on the model outputs. It demonstrated that the rice growth was easily affected by the changes of climate conditions at the vegetative phase regardless of the different cultivars (Figure 4). In phenology-related parameters, P2O was the most sensitive parameter for the model outputs. The result agreed with the global SA when the variation of climate parameters occurred during the whole growth season (Figure 7). At panicle-formation phase, climate parameters indicated no effects on the model outputs, which was likely due to the small duration length of this phase (4–5 days) which had negligible influence on the accumulation of degree days. At the ripening phase, climate parameters showed no influence on ADAP (Figure 6), which was because ADAP was only controlled by the accumulation of thermal time from planting to flowering. The effects of climate parameters on different cultivar types were not completely concordant. For instance, parameter $T_{avg}$ in late-season and one-season-late cultivars showed a considerable effect on MDAP ($ST_i > 0.1$); while $T_{avg}$ in mid-season cultivars indicated no significant effect on MDAP ($ST_i < 0.05$). In general, the sensitivity rankings of the parameters were similar under variations of climate parameters at the panicle-formation phase and ripening phase (Figures 5–7).

Cultivars with environment studies have been conducted such as investigations of ideal cultivars for the given environments for rice [51] and wheat [52], as well as investigations of genetic gains in soybean for given possible sources [53]. However, due to the variation of irrigation, fertilization, and soil conditions, these factors could bring large uncertainty as well as interactions for the global SA. In this study, all the investigated cultivars were planted in the same site with the same field management and soil conditions; we only analyzed the effects of inter-cultivars and cultivar types for the model outputs with variation of climate parameters at specific stages, which allowed for testing the CERES-Rice model responses to the changes of cultivars and climate status as well as utilizing genotypes in the currently explored conditions in the breeding trials. The ideal cultivars in different locations might be related to different climate conditions. Therefore, the variations of climate conditions at specific phases should be considered in selecting reasonable cultivar types in rice breeding.
Figure 7. The main total sensitivity indices ($ST_i > 0.05$ at the whole growth season) for the model outputs under the specific-stage variations of climate parameters. (a,e,i), (b,f,j), (c,g,k), and (d,h,l) represent the main influential parameters for model outputs (ADAP, MDAP, and yield) under variations of climate parameters for the whole growth season, vegetative phase, panicle-formation phase, and ripening phase, respectively.

5. Conclusions

The Sobol’ method was applied to investigate the effects of cultivars and different specific-stage variations of climate parameters on parameter sensitivity in the CERES-Rice model. The global SA demonstrated that the variation of climate parameters was: (1) for the whole rice growth season, the interactions between parameters were larger than the effects of the parameters themselves for the model outputs and different cultivar types showed no significant effects on parameter rankings ($p < 0.05$); (2) at the vegetative phase, Tavg indicated a considerable effect on the variation of all the model outputs; (3) at the panicle-formation phase, the climate parameters demonstrated no effect on model outputs ($ST_i < 0.05$); (4) and at the ripening phase, ADAP were only affected by phenology-related parameters while Tavg showed different effects on MDAP depending on the cultivar types. Additionally, the species parameter PORM indicated an indispensable influence on yield regardless of the different specific-stage variations of the climate conditions ($ST_i > 0.05$). In all, these investigations provided useful knowledge to guide efforts toward model calibration and applications in rice breeding trials.
Author Contributions: Conceptualization, H.G.; methodology, H.G.; investigation, C.D., H.G., F.M., and Z.L.; resources, C.D.; data curation, H.G.; writing—original draft preparation, H.G.; writing—review and editing, C.D.; visualization, H.G.; supervision, C.D. All authors have read and agreed to the published version of the manuscript.

Funding: This study was supported by the Key Research and Development Program of Shandong Province (2019JZZY010713), National Key Research and Development Program of China (No. 2018YFE0107000), and Blue Project of Jiangsu Province.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Data sharing not applicable.

Acknowledgments: Thanks go to Jingyou Guo and Youdong Hu for providing the details of the experimental design in this study.

Conflicts of Interest: The authors declare no conflict of interest.

Appendix A

Table A1. Cultivar parameters range of the CERES-Rice model.

| Parameter | Description                                                                 | Unit     | Range   |
|-----------|------------------------------------------------------------------------------|----------|---------|
| P1        | Time period in °C above a base temperature of 9 °C during the basic vegetative phase | GDD (°C) | 210–900 |
| P2O       | Critical photoperiod (in hours) at which the development occurs at a maximum rate | hours    | 10.4–13 |
| P2R       | Extent to which phasic development leading to panicle initiation is delayed for each hour increase in photoperiod above P2O | GDD h⁻¹ | 30–200  |
| G1        | Potential spikelet number coefficient                                        | –        | 50–80   |
| G3        | Tillering coefficient relative to IR64 cultivar under ideal conditions      | –        | 0.3–1   |
| G4        | Temperature tolerance coefficient                                            | –        | 0.8–1.25|

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