BIDIRECTIONAL PARSING OF LEXICALIZED TREE ADJOINING GRAMMARS*

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Abstract

In this paper a bidirectional parser for Lexicalized Tree Adjoining Grammars will be presented. The algorithm takes advantage of a peculiar characteristic of Lexicalized TAGs, i.e. that each elementary tree is associated with a lexical item, called its anchor. The algorithm employs a mixed strategy: it works bottom-up from the lexical anchors and then expands (partial) analyses making top-down predictions. Even if such an algorithm does not improve the worst-case time bounds of already known TAGs parsing methods, it could be relevant from the perspective of linguistic information processing, because it employs lexical information in a more direct way.

1. Introduction

Tree Adjoining Grammars (TAGs) are a formalism for expressing grammatical knowledge that extends the domain of locality of context-free grammars (CFGs). TAGs are tree rewriting systems specified by a finite set of elementary trees (for a detailed description of TAGs, see (Joshi, 1985)). TAGs can cope with various kinds of unbounded dependencies in a direct way because of their extended domain of locality; in fact, the elementary trees of TAGs are the appropriate domains for characterizing such dependencies. In (Kroch and Joshi, 1985) a detailed discussion of the linguistic relevance of TAGs can be found.

Lexicalised Tree Adjoining Grammars (Schabes et al., 1988) are a refinement of TAGs such that each elementary tree is associated with a lexical item, called the anchor of the tree. Therefore, Lexicalized TAGs conform to a common tendency in modern theories of grammar, namely the attempt to embed grammatical information within lexical items. Notably, the association between elementary trees and anchors improves also parsing performance, as will be discussed below.

Various parsing algorithms for TAGs have been proposed in the literature: the worst-case time complexity varies from $O(n^4 \log n)$ (Harbusch, 1990) to $O(n^3)$ (Vijay-Shanker and Joshi, 1985, Lang, 1990, Schabes, 1990) and $O(n^2)$ (Schabes and Joshi, 1988). As for Lexicalized TAGs, in (Schabes et al., 1988) a two step algorithm has been presented: during the first step the trees corresponding to the input string are selected and in the second step the input string is parsed with respect to this set of trees. Another paper by Schabes and Joshi (1989) shows how parsing strategies can take advantage of lexicalization in order to improve parsers' performance. Two major advantages have been discussed in the cited work: grammar filtering (the parser can use only a subset of the entire grammar) and bottom-up information (further constraints are imposed on the way trees can be combined). Given these premises and starting from an already known method for bidirectional CF language recognition (Satta and Stock, 1989), it seems quite natural to propose an anchor-driven bidirectional parser for Lexicalized TAGs that tries to make more direct use of the information contained within the anchors. The algorithm employs a mixed strategy: it works bottom-up from the lexical anchors and then expands (partial) analyses making top-down predictions.

2. Overview of the Algorithm

The algorithm that will be presented is a recognizer for Tree Adjoining Languages: a parser can be obtained from such a recognizer by additional processing (see final section). As an introduction to the next section, an informal description of the studied algorithm is here presented. We assume the following definition of TAGs.

**Definition 1** A Tree Adjoining Grammar (TAG) is a 5-tuple $G = (V_N, V_S, S, I, A)$, where $V_N$ is a finite set of non-terminal symbols, $V_S$ is a finite set of terminal symbols, $S \in V_N$ is the start symbol, $I$ and $A$ are two finite sets of trees, called initial trees and auxiliary trees respectively. The trees in the set $I \cup A$ are called elementary trees.

We assume that the reader is familiar with the definitions of adjoining operation and foot node (see (Joshi, 1985)).

The proposed algorithm is a tabular method that accepts a TAG $G$ and a string $w$ as input, and decides whether $w \in L(G)$. This is done by recovering (partial) analyses for substrings of $w$ and by combining them. More precisely, the algorithm factorizes analyses of derived trees by employing a specific structure called state. Each state retains a pointer to a node $n$ in some tree $\alpha \in I \cup A$, along with two additional pointers (called idot and rdot) to $n$ itself or to

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its children in $\alpha$. Let $\alpha_n$ be a tree obtained from the
maximal subtree of $\alpha$ with root $n$, by means of
some adjoining operations. Informally speaking and
with a little bit of simplification, the two following
cases are possible. First, if $ldot, rdot \in \alpha$, state $s$
indicates that the part of $\alpha_n$ dominated by the nodes
between $ldot$ and $rdot$ has already been analyzed by
the algorithm. Second, if $ldot=rdot=n$, state $s$
indicates that the whole of $\alpha_n$ has already been analyzed,
including possible adjunctions to its root node $n$.

Each state $s$ will be inserted into a recognition
matrix $T$, which is a square matrix indexed from 0 to
$n_w$, where $n_w$ is the length of $w$. If state $s$
belongs to the component $t_{i,j}$ of $T$, the partial analysis
(the part of $\alpha_n$) represented by $s$ subsumes the substring
of $w$ that starts from position $i$ and ends at position $j$,
except for the items dominated by a possible foot
node in $\alpha_n$ (this is explicitly indicated within $s$).

The algorithm performs the analysis of $w$ start-
ing from the anchor node of every tree in $G$ whose
category is the same as an item in $w$. Then it tries to
extend each partial analysis so obtained, by climbing
each tree along the path that connects the anchor
node to the root node; in doing this, the algorithm
recognizes all possible adjunctions that are present
in $w$. Most important, every subtree $\gamma$ of a tree derived
from $\alpha \in \Delta A$, such that $\gamma$ does not contain the
anchor node of $\alpha$, is predicted and analyzed by the algo-
rithm in a top-down fashion, from right to left (left
to right) if it is located to the left (right) of the path
that connects the anchor node to the root node in $\alpha$.

The combinations of partial analyses (states) and
the introduction of top-down prediction states is car-
ried out by means of the application of six proce-
dures that will be defined below. Each procedure ap-
plies to some states, trying to “move” outward one
of the two additional pointers within each state.

The algorithm stops when no state in $T$ can be
further expanded. If some state has been obtained that
subsumes the input string and that represents a com-
plete analysis for some tree with the root node of
category $S$, the algorithm succeeds in the recogni-
tion.

3. The Algorithm

In the following any (elementary or derived) tree
will be denoted by a pair $(N, E)$, where $N$ is a finite
set of nodes and $E$ is a set of ordered pairs of nodes,
called arcs. For every tree $\alpha=(N, E)$, we define five
functions of $N$ into $N \cup \{\bot\}$, 1 called father, leftmost-
child, rightmost-child, left-sibling, and right-sibling
(with the obvious meanings). For every tree $\alpha=(N, E)$
and every node $n \in N$, a function $\text{domain}_n(\alpha)$ is
defined such that $\text{domain}_n(\alpha)=\beta$, where $\beta$ is the maxi-
mal subtree in $\alpha$ whose root is $n$.

For any $TAG G$ and for every node $n$ in some
tree in $G$, we will write $\text{cat}(n)=X$, $X \in V_N \cup V_S$
whenever $X$ is the symbol associated to $n$ in $G$.

1The symbol “$\bot$” denotes here the undefined element.
The algorithm that will be presented employs the following function.

Definition 3 A function is defined as follows:
\[ F: \mathcal{P}(A) \rightarrow \mathcal{P}(\mathcal{A}) \]
\[ F(a) = \{ s | s = (\text{father}(n), n, \text{left}, n, \text{right}, \ldots) \text{ for some } n \in A \} \]

The details of the algorithm are as follows.

Algorithm 1
Let \( G = (V_N, V_S, s, I, A) \) be a TAG and let \( w = a_1 \ldots a_m, n_w \geq 1 \), be any string in \( V_S^* \). Let \( T \) be a recognition matrix of size \((n_w+1) \times (n_w+1)\) whose components \( t_{ij} \) are indexed from 0 to \( n_w \) for both sides. Develop matrix \( T \) in the following way (a new state \( s \) is added to some entry in \( T \) only if \( s \) is a subset of any string in \( V_A^* \). Let \( T \) be the recognition matrix of size \((n_w+1) \times (n_w+1)\) whose components \( t_{ij} \) are indexed from 0 to \( n_w \) for both sides. Develop matrix \( T \) in the following way (a new state \( s \) is added to some entry in \( T \) only if \( s \) is a subset of any string in \( V_A^* \).

1. For every state \( s \) where \( F(a) \), \( 1 \leq s \leq n_w \), add \( s \) to \( t_{i,j} \).
2. Process each state \( s \) added to some entry in \( T \) by means of the following procedures in any order:
   - **Left-expander(s)**, **Right-expander(s)**,
   - **Move-dot-left(s)**, **Move-dot-right(s)**,
   - **Completer(s)**, **Adjoiner(s)**,
   - until no state can be further added.
3. If \( s = [n, n, \text{left}, n, \text{right}, \ldots] \) for some node \( n \) such that \( \text{cat}(n) = \alpha \) and \( \text{cat}(\alpha) = \beta \) for some tree \( \alpha \in \mathcal{P}(\mathcal{A}) \).

The six procedures mentioned above are defined in the following.

Procedure 1 **Left-expander**
Input A state \( s = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \)
in \( t_{i,j} \).
Precondition \( m \neq \text{lm} \), \( \text{ldot} \neq \alpha \), and \( \text{ldot} \neq \text{right} \).
Description
Case 1: \( \text{ldot} \neq \epsilon \).
Assume \( a_{\text{ldot}} = \text{cat}(\text{ldot}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Case 2: \( \text{ldot} = \text{ldot} \).
If \( a_{\text{ldot}} = \text{cat}(\text{ldot}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Procedure 2 **Right-expander**
Input A state \( s = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \)
in \( t_{i,j} \).
Precondition \( m \neq \text{rm} \), \( \text{rpos} \neq \text{left} \), and \( \text{rpos} \neq \text{right} \).
Description
Case 1: \( \text{rpos} \neq \epsilon \).
Assume \( a_{\text{rpos}} = \text{cat}(\text{rpos}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Case 2: \( \text{rpos} = \text{rpos} \).
If \( a_{\text{rpos}} = \text{cat}(\text{rpos}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Procedure 3 **Move-dot-left**
Input A state \( s = [n, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \)
in \( t_{i,j} \).
Precondition \( m \neq \text{lm} \), \( \text{ldot} \neq \alpha \), and \( \text{ldot} \neq \text{right} \).
Description
Case 1: \( \text{ldot} = \text{ldot} \).
Assume \( a_{\text{ldot}} = \text{cat}(\text{ldot}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Case 2: \( \text{ldot} = \epsilon \).
If \( a_{\text{ldot}} = \text{cat}(\text{ldot}) \), add state \( s' = [n, \text{ldot}, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Procedure 4 **Move-dot-right**
Input A state \( s = [n, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \)
in \( t_{i,j} \).
Precondition \( m \neq \text{rm} \), \( \text{rpos} \neq \text{left} \), and \( \text{rpos} \neq \text{right} \).
Description
Case 1: \( \text{rpos} = \text{rpos} \).
Assume \( a_{\text{rpos}} = \text{cat}(\text{rpos}) \), add state \( s' = [n, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).

Case 2: \( \text{rpos} = \epsilon \).
If \( a_{\text{rpos}} = \text{cat}(\text{rpos}) \), add state \( s' = [n, \text{ldot}, \text{rdot}, \text{rpos}, \text{fr}, \text{m}] \) to \( t_{i,j} \).
Procedure 5 Completer

Input A state $s=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$.

Precondition $n$ is not the root of an auxiliary tree.

Description

Case 1: $n$ Middle-nodes, $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$.

Add state $s_0=\{\text{father}(n), l, r, f_l, f_r, m\}$ to $t_i$. $j$.

Case 2: $n$ Left-nodes.

For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $l$; $r$ is not the root of an auxiliary tree, and $m_0=\text{lm}$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$; if left-expansion is successful for state $s_0$, set $m_0=\text{lm}$ in $s_0$.

Case 3: $n$ Right-nodes.

For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $l$; $r$ is not the root of an auxiliary tree, and $m_0=\text{lm}$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$; if right-expansion is successful for state $s_0$, set $m_0=\text{rm}$ in $s_0$.

Procedure 6 Adjoiner

Input A state $s=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$.

Precondition Void.

Description

Case 1: apply always.

For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $l$; $r$ is not the root of an auxiliary tree, and $m_0=\text{lm}$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$.

Case 2: $n$ is the root of an auxiliary tree.

Step 1: For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $n=\text{Adjoin}(n)$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$.

Step 2: For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $n=\text{Adjoin}(l)$ or $m=\text{lm}$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$.

Step 3: For every state $s_0=\{n, l, r, f_l, f_r, m\}$ in $t_i$. $j$; $i<j$, such that $n=\text{Adjoin}(r)$ and $m=\text{rm}$, add state $s_0=\{n, l, r, f_l, f_r, m\}$ to $t_i$. $j$.

4. Formal Results

Some definitions will be introduced in the following, in order to present some interesting properties of Algorithm 1. Formal proofs of the statements below can be found in (Satta, 1990).

Let $n$ be a node in some tree $\alpha \in \mathcal{A}$, Each state $s=\{n, l, r, f_l, f_r, m\}$ in $\mathcal{I}_S$ identifies a tree forest $\phi(s)$ composed of all maximal subtrees in $\alpha$ whose roots are "spanned" by the two positions $l$ and $r$. If $l$ is not in $\{l, r, f_l, f_r, m\}$ in $\mathcal{I}_S$, $\phi(s)$ is defined as the maximal subtree in $\alpha$ whose root is included in $\phi(s)$ if and only if $l$ is the left of $r$ (the mirror case holds w.r.t. $r$). We define the subsumption relation $\subseteq$ on $\mathcal{I}_S$ as follows: $s \subseteq s'$ iff state $s$ has the same first component as state $s'$ and $\phi(s)$ is included in $\phi(s')$. We also say that a forest $\phi(s)$ derives a forest $\psi$ ($\phi(s) \triangleright \psi$) whenever $\phi(s)$ can be obtained from $\phi(s')$ by means of some adjoining operations. Finally, $E$ denotes the immediate dominance relation on nodes of $\alpha \in \mathcal{A}$, and $\pi(\alpha)$ denotes the foot node of $\alpha$ (if $\alpha \in \mathcal{A}$).

The following statement characterizes the set of all states inserted in $T$ by Algorithm 1.

Theorem 1 Let $n$ be a node in $\alpha \in \mathcal{A}$ and let $n'$ be the lowest node in $\beta \in \mathcal{A}$ such that $\alpha \subseteq n'$ and $n' \in \mathcal{I}_S$; let also $s=\{n, l, r, f_l, f_r, m\}$ be a state in $\mathcal{I}_S$. Algorithm 1 inserts a state $s'$ such that $s \leq s'$, in $t_i$. $h_1$, $h_2 \geq 0$, if and only if one of the following conditions is met:

(i) $n \in \text{Middle-nodes}(n'=n')$ and $\phi(s) \triangleright \psi$, where $\psi$ spans $a_{i+1}$ ... $a_j$ (with the exception of string $a_{i+1}$ ... $a_f$ if $\pi(\alpha)$ is included in $\phi(s)$) (see Figure 1);

(ii) $n \in \text{Left-nodes}(s=s'$, $h_1=h_2=0$ and $\phi(s) \triangleright \psi'$, where $\psi'$ spans $a_{i+1}$ ... $a_j$ (with the exception of string $a_{i+1}$ ... $a_f$ if $\pi(\alpha)$ is included in $\phi(s)$). Moreover, $n'$ is the root of a (maximal) subtree $\tau$ in $\alpha$ such that $\tau \subseteq \psi$, $\psi'$ strictly includes $\psi'$ and every tree $\beta \in \mathcal{A}$ that has been adjoined to some node in the path from $n'$ to $n$ spans a string that is included in $a_1$ ... $a_j$ (see Figure 2);

(iii) the symmetrical case of (ii).

In order to present the computational complexity of Algorithm 1, some norms for TAGs are here introduced. Let $\mathcal{A}$ be a set of nodes in some trees of a TAG $G$; we define

$$|G|_{\mathcal{A}, k} = \sum_{n \in \mathcal{A}} \text{children}(n)^k.$$
Theorem 2 If some auxiliary structures (vector of lists) are used by Algorithm 1 for the bookkeeping of all states that correspond to completely analyzed auxiliary trees, a string can be recognized in \( O(n^t.\lambda t.\max\{|G|, |M|, 1 + |G| + |M|\}) \) time, where \( M = \text{Middle-nodes} \) and \( X \) denotes the set of all nodes in the trees of \( G \).

5. A Linguistic Example

In order to gain a better understanding of Algorithm 1 and to emphasize the linguistic relevance of TAGs, we present a running example. In the following we assume the formal framework of X-bar Theory (Jackendoff, 1977). Given the sentence:

(1) Gianni incontra Maria per caso

lit. Gianni meets Maria by chance

we will propose here the following analysis (see Figure 4):

(2) \([\text{CP} [\text{IP} [\text{NP Gianni} [\text{incontra [\text{VP [\text{we i [\text{~ Maria}]} [\text{pp per caso}]]]}]]]]]])

Note that the Verb \textit{incontra} has been moved to the Inflection position. Therefore, the PP adjunction stretches the dependency between the Verb \textit{incontra} and its Direct Object \textit{Maria}. These cases may raise some difficulties in a context-free framework, because the lack of the head within its constituent makes the task of predicting the object(s) rather inefficient.

Assume a TAG \( G=(V_N, V_{\Sigma}, S, I, A) \), where \( V_N=\{\text{IP, I', VP, V', NP}\} \), \( V_{\Sigma}=\{\text{Gianni, Maria, incontra, PP}\} \), \( I=\{\alpha\} \) and \( A=\{\beta\} \) (see Figure 3; each node has been paired with an integer which will be used as its address). In order to simplify the computation, we have somewhat reduced the initial tree \( \alpha \) and we have considered the constituent PP as a terminal symbol. In Figure 4 the whole analysis tree corresponding to (2) is reported.

Let \( \tau(\alpha)=5 \), \( \tau(\beta)=13 \); from Definition 3 it follows that:

\[
F(5)=[\{4, 5, \text{left}, 5, \text{right}, \cdot, \cdot, \cdot\}], \\
F(13)=[\{11, 13, \text{left}, 11, \text{right}, \cdot, \cdot, \cdot\}].
\]

A run of Algorithm 1 on sentence (1) is simplified in the following steps (only relevant steps are reported).

First of all, the two anchors are recognized:

1) \( s_1=[4, 5, \text{left}, 5, \text{right}, \cdot, \cdot, \cdot] \) is inserted in \( t_{1,2} \) and \( s_2=[11, 13, \text{left}, 13, \text{right}, \cdot, \cdot, \cdot] \) is inserted in \( t_{3,4} \) by line 1 of the algorithm.

Then, auxiliary tree \( \beta \) is recognized in the following steps:

2) \( s_3=[11, 12, \text{right}, 13, \text{right}, \cdot, \cdot, \cdot] \) is inserted in \( t_{3,4} \) and \( m \) is set to \( rm \) in state \( s_4 \), by Case 2 of the \textit{move-dot-left} procedure;

3) \( s_4=[11, 12, \text{left}, 13, \text{right}, 2, 3, \cdot] \) is inserted in \( t_{2,4} \) and \( m \) is set to \( rm \) in state \( s_5 \), by Case 3 of the \textit{left-expander} procedure;

4) \( s_5=[11, 11, \text{left}, 13, \text{right}, 2, 3, \cdot] \) is inserted in \( t_{2,4} \) and \( m \) is set to \( rm \) in state \( s_4 \), by Case 3 of the \textit{move-dot-left} procedure;

5) \( s_9=[11, 11, \text{left}, 11, \text{right}, 2, 3, \cdot] \) is inserted in \( t_{3,4} \) and \( m \) is set to \( lm \) in state \( s_5 \), by Case 3 of the \textit{move-dot-right} procedure.

\[
\alpha:
\begin{array}{c}
\text{IP} (1) \\
\text{NP} (2) \\
\text{Gianni incontra} (3) \\
\text{VP} (4) \\
\text{e i} (5) \\
\text{NP} (6) \\
\text{Maria} (7) \\
\text{VP} (8) \\
\text{PP} (9) \\
\text{per caso} (10)
\end{array}
\]

\[
\beta:
\begin{array}{c}
\text{IP} (1) \\
\text{NP} (2) \\
\text{Gianni incontra} (3) \\
\text{VP} (4) \\
\text{e i} (5) \\
\text{NP} (6) \\
\text{Maria} (7) \\
\text{VP} (8) \\
\text{PP} (9) \\
\text{per caso} (10)
\end{array}
\]

After the insertion of state \( s_9=[6, 6, \text{left}, 6, \text{left}, \cdot, \cdot, \cdot] \) in \( t_{2,4} \) by Case 2 of the \textit{move-dot-right} procedure, the VP node (6) is hypothesized by Case 1 (Step 2, via state \( s_6 \)) of the \textit{right-expander} procedure with the insertion of state \( s_9=[6, 6, \text{left}, 6, \text{left}, \cdot, \cdot, \cdot] \) in \( t_{2,4} \). The whole recognition of node (6) takes place with the insertion of state \( s_9=[6, 6, \text{left}, 6, \text{right}, \cdot, \cdot, \cdot] \) in \( t_{2,4} \). Then we have the following step:

6) \( s_{10}=[6, 6, \text{left}, 6, \text{right}, \cdot, \cdot, \cdot] \) is inserted in
$t_{2,4}$, by the adjoiner procedure.
The analysis proceeds working on tree $\alpha$ and reaching a final configuration in which state $s_{11}=[1, 1, left, 1, right, -, -]$ belongs to $t_{0,4}$.

6. Discussion

Within the perspective of Lexicalized TAGs, known methods for TAGs recognition/parsing present some limitations: these methods behave in a left-to-right fashion (Schabes and Joshi, 1988) or they are purely bottom-up (Vijay-Shanker and Joshi, 1985, Harbusch, 1990), hence they cannot take advantage of anchor information in a direct way. The presented algorithm directly exploits both the advantages of lexicalization mentioned in the paper by Schabes and Joshi (1989), i.e. grammar filtering and bottom-up information. In fact, such an algorithm starts partial analyses from the anchor elements, directly selecting the relevant trees in the grammar, and then it proceeds in both directions, climbing to the roots of these trees and predicting the rest of the structures in a top-down fashion. These capabilities make the algorithm attractive from the perspective of linguistic information processing, even if it does not improve the worst-case time bounds of already known TAGs parsers.

The studied algorithm recognizes auxiliary trees without considering the substring dominated by the foot node, as is the case of the CYK-like algorithm in Vijay-Shanker and Joshi (1985). More precisely, Case 3 in the procedure Left-expander nondeterministically jumps over such a substring. Note that the alternative solution, which consists in waiting for possible analyses subsumed by the foot node, would prevent the algorithm from recognizing particular configurations, due to the bidirectional behaviour of the method (examples are left to the reader). On the contrary, Earley-like parsers for TAGs (Lang, 1990, Schabes, 1990) do care about substrings dominated by the foot node. However, these algorithms are forced to start at each foot node the recognition of all possible subtrees of the elementary trees whose roots can be the locus of an adjunction.

In this work, we have discussed a theoretical schema for the parser, in order to study its formal properties. In practical cases, such an algorithm could be considerably improved. For example, the above mentioned guess in Case 3 of the procedure Left-expander could take advantage of look-ahead techniques. So far, we have not addressed topics such as substitution or on-line recognition. Our algorithm can be easily modified in these directions, adopting the same proposals advanced in (Schabes and Joshi, 1988).

Finally, a parser for Lexicalized TAGs can be obtained from Algorithm 1. To this purpose, it suffices to store elements in $t_{35}$ into the recognition matrix $T$ along with a list of pointers to those entries that caused such elements to be placed in the matrix. Using this additional information, it is not difficult to exhibit an algorithm for the construction of the desired parser(s).

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