Elgin, Ceyhun; Kuzubas, Tolga Umut

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Wage-Productivity Gap in OECD Economies

Ceyhun Elgin and Tolga Umut Kuzubas

Abstract
The Walrasian theory of labor market equilibrium predicts that in the absence of any market frictions, workers earn a wage rate equal to their marginal productivity. In this paper, based on the neoclassical tradition, the authors define the ratio of the marginal product of labor to real wages as the Pigouvian exploitation rate and then construct a panel dataset of this specific wage-productivity gap for the manufacturing sector in OECD economies. Next, they investigate its relationship with the unemployment rate along with various other variables such as the government taxation, capital expansion, unionization, inflation. Their findings suggest that the wage-productivity gap gives a robust and significantly positive response to shocks to unemployment rate and a negative response to shocks to unionization.

JEL J24 J30 J64
Keywords Wages; marginal productivity of labor; panel-VAR; OECD economies

Authors
Ceyhun Elgin, Bogazici University, Department of Economics, Natuk Birkan Building, 34342 Bebek, Istanbul, Turkey, ceyhun.elgin@boun.edu.tr
Tolga Umut Kuzubas, Bogazici University, Department of Economics, Natuk Birkan Building, 34342 Bebek, Istanbul, Turkey, umut.kuzubas@boun.edu.tr

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1 Introduction

In the absence of any market distortions, the assumptions of the existence of perfect competition in the labor market and profit maximizing behavior of firms under constant returns to scale imply that real wages should be equal to the marginal product of labor (MPL). When competitive firms take product and factor prices as given and maximize their profit function, it is immediate from the profit maximization behavior of the firm that the real wages should equal the marginal product of labor. However, this theoretical result is not supported empirically for various economies. For example, in Elgin and Kuzubas (2012) we investigate the evolution of the relationship between the real wages and the marginal product of labor in the Turkish manufacturing sector and find that there is a significant gap between these two variables. More importantly, using different time-series techniques we also find that this gap is foremost affected by the unemployment rate in Turkey.

Aiming to generalize this result, in this paper we conduct this analysis using a cross-country panel data set consisting of 31 countries over a time span of 50 years between 1960 and 2009. Specifically, we investigate the interaction of the wage-productivity gap with various other variables. The availability of a panel dataset allows us to examine both the cross-country and time-series variation in the wage-productivity gap. In order to understand how the wage-productivity gap is related to several other variables, we use the Panel-VAR approach a la Holtz-Eakin et al. (1988) to capture possible endogeneity between the wage-productivity gap and the variables potentially affecting this gap. We examine the effects of unemployment rate, capital deepening, unionization, inflation on the wage-productivity gap. Among these four variables, our empirical results indicate that the wage-productivity gap gives a robust and significantly positive response to shocks to unemployment and a negative response to shocks to unionization.

The rest of the paper is organized as follows: In the next section, we briefly describe how our paper is related to both the empirical and the theoretical literature by focusing on the contribution of our paper. Next, in Section 3 we outline the theoretical framework behind our analysis. Section 4 then presents the methodology and results of the empirical analysis and finally, Section 5 concludes.
2 Related Literature

The Walrasian theory of labor market equilibrium predicts that in the absence of any distortions, workers should earn a wage rate which is equal to their marginal product, measured in units of output. Among other factors, our main focus in this paper is to uncover the relationship between the real wages and the unemployment rate. In a competitive labor market without any frictions, the observed wage-productivity gap is an outcome of temporary disequilibrium dynamics which should disappear in the long-run. The rationale behind this prediction is that, when wages are below the productivity level of workers, firms will have an incentive to hire more workers. This will put an upward pressure on wages and if wages are above the marginal product, it will be profitable for the firm to reduce the labor. This will then drive wages down. Therefore, the existence of an equilibrium in the labor market requires that wages should be equal to the marginal product of labor. The empirical literature relying on the competitive markets investigates wage-productivity gap as a determinant of unemployment. For example, Bruno and Sachs (1985) identify the increase in the wage-productivity gap as the main determinant of high unemployment rates in OECD countries during the 1970’s. Gordon (1995), on the other hand, provides evidence that there is no cross-country correlation between these two variables in the 1980’s. Following these studies, an extensive literature analyzing the wage-productivity gap as a determinant of unemployment emerged\(^1\) and found little empirical support on the effect of wage-productivity gap on unemployment. One exception is Lopez-Villavicencio and Silva (2011) who reestablish this empirical result by introducing labor market regulations.

Another way to think about the theoretical predictions is to rely on the models which explicitly account for the frictions in the labor market. For example, considering the benchmark Mortensen-Pissarides model,\(^2\) the observed gap between wages and productivity could be determined by the bargaining powers of the workers and aggregate labor market conditions. Supporting our results, this model predicts a positive correlation between the wage-productivity gap and unem-

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\(^1\) Also see Junankar and Madsen (2004), Pascalau (2007), Madsen (1994).

\(^2\) See Pissarides (2000) for a discussion.
ployment simply because a higher unemployment rate reduces the outside option of the workers in their bargaining process with the firm and push them to settle for lower wages. On the other hand, Shimer (2009) and Blanchard and Gali (2010) argue that under certain assumptions productivity shocks translate into proportional changes in wages. This result suggests that the theoretical correlation between the wage-productivity gap and unemployment should be zero. In the search-theoretic literature, this observation is related to the so-called "Shimer puzzle" where positive productivity shocks are absorbed by wage increases due to the Nash-bargaining assumptions and do not generate the response in the aggregate unemployment observed in the data.³ On the other hand, by introducing sticky wages, i.e. limited response of wages to productivity shocks, Hall (2005) generates a positive effect on the unemployment. Our analysis can be thought as an empirical test whether this correlation is significantly different from zero or not.⁴

This prediction is not tested by the empirical literature described above because it generally treats the wage-productivity gap as exogenous when examining the relationship between these two variables. However, the theory suggests a two-way causation between the wage-productivity gap and unemployment. In this regard, this paper is an attempt to fill in this gap in the empirical literature by relying on Panel-VAR techniques.

### 3 Theoretical Framework

In the introduction, we briefly discuss the theoretical predictions on the relationship between wage-productivity gap and unemployment. Walrasian theory has been extensively analyzed by the empirical literature however the effect of search and

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³ The model generates a very small positive correlation between productivity shocks and unemployment when calibrated to the US economy.

⁴ The search-theoretic literature on labor markets assumes that wages are determined through a Nash-bargaining procedure with fixed bargaining powers. This assumption makes wages too responsive to productivity changes and is the main driving force behind the low correlation between the wage-productivity gap and unemployment. Actually, the effect of the unemployment on wages becomes more significant, if we tie the bargaining power of the workers to aggregate unemployment rates. See Elgin and Kuzubas (2012) for a version of a bargaining game which derives the bargaining power of the workers as a function of the aggregate unemployment rate.
bargaining frictions on this relationship received relatively less attention. In this section, we elaborate the predictions of the literature by relying on the well-established Mortensen-Pissarides framework.

In this type of models, wages are determined as an outcome of Nash-bargaining between workers and firms. Therefore, they are related to bargaining powers and the outside options which are determined by the labor market conditions. Note that this type of wage-determination reduces the wage-productivity gap when we give all the bargaining power to the worker and in the opposite case, any positive bargaining power of the firm will lead to a higher gap. This shows that the bargaining power is critical in determining the size of the wage-productivity gap implied by the model. The unemployment rate on the other hand, affects the wages through its indirect effect on the outside options of workers. In other words, a higher unemployment rate reduces the job finding rates of the workers and hence their outside options, therefore, workers will settle for a lower wage. Taking productivity as given, this will increase the wage-productivity gap. So according to this mechanism, the bargaining power and unemployment will be the main determinants of the wage-productivity gap.

In another paper, Elgin and Kuzubas (2012), we link the bargaining power of the worker (which is usually treated as exogenous in these type of models) to the unemployment rate by introducing a bargaining game between the worker and the firm to the standard Mortensen-Pissarides framework in the line of Cahuc, Postel-Vinay and Robin (2003). We derive the bargaining power of the workers as a function of the unemployment rate and show that there is a negative relationship between the bargaining power and unemployment rate. Noticeably, this reinforces the effect of unemployment on the wage-productivity gap.

The theoretical mechanism we have outlined above suggests that, combining with the Walrasian equilibrium, there is a possible two-way causation between the wage-productivity gap and unemployment. However, the empirical literature focusing on the effect of wage-gap on unemployment mostly neglects the unemployment as a determinant of the wage-productivity gap and is not consistent with this theoretical prediction. This negligence calls for an empirical analysis to account for this observation. Also, a robust empirical analysis should control for the factors which potentially affect the bargaining power of the workers such as the unionization rate. That is why we conduct an empirical analysis controlling
for the possible two-way causation and country specific effects with a rich set of control variables using a Panel-VAR framework in our estimation.

4 Empirical Analysis

4.1 Methodology

We use panel-data vector autoregression (VAR) methodology which fits the purpose of this paper well as the theoretical predictions indicate a two-way causation between wage-productivity gap and unemployment rate.\(^5\) The Panel-VAR framework extends the traditional VAR approach to a panel data setting and allows us to control for country level heterogeneity. In the estimated model, we treat both wage-productivity gap and unemployment as endogenous (along with potential other variables such as unionization, inflation and capital deepening) and pose the following specification:

\[
y_{it} = \sum_{j=1}^{p} \beta_j y_{i,t-j} + \sum_{j=1}^{p} \delta_j x_{i,t-j} + f_i + \nu_{it}
\]

where \(y_{it}\) is the set of endogenous variables used in the estimation, i.e. wage-productivity gap and unemployment along with unionization, inflation and capital deepening in extended estimations. \(x_{it}\) represents the set of covariates, and \(f_i\) stands for unobserved country level effects.

Applying the VAR methodology to panel data presents a problem associated with lagged dependent variables in both fixed and random effects settings. In order to address this problem we use the methodology proposed by Holtz-Eakin (1988). In the traditional VAR setting, one needs to impose the restriction that the data generating process is the same for each cross-section of observation which usually does not hold. Therefore, in order to control for country level heterogeneity we introduce fixed effects, \(f_i\) in the model. In the VAR setting, because of the

\(^5\) We also run several static and dynamic panel-data estimations where we use the wage-productivity gap as the dependent variable of the regressions. In these estimations we obtained qualitatively somewhat similar results. These are available upon request from the corresponding author.
dynamic nature of the estimation, lagged dependent variables are correlated with
the disturbance term. For the fixed effect estimator transformation of variables
eliminates \( f_i \) however, the regressor \( y_{it-1} - \bar{y}_{i,t-1} \), with \( \bar{y}_{i,t-1} = \sum_{t=p+1}^{T} y_{it-1} / (T - p) \),
will still be correlated with the error term \( v_{it} - \bar{v}_i \), where \( \bar{v}_i = \sum_{t=p+1}^{T} v_{it} / (T - p) \), because \( y_{it-1} \) is correlated with \( \bar{v}_i \) by construction. Therefore, the mean-
differencing procedure commonly used to eliminate fixed effects would create
biased coefficients especially with a limited number of time-series observations.
In order to eliminate this problem, we use forward mean-differencing, known as
the "Helmert procedure". This procedure only subtracts the mean of all the future
observations available for each country-year. This transformation satisfies the
orthogonality assumption between transformed variables and lagged regressors.
Therefore, we can use lagged dependent variables as instruments and estimate the
coefficients by system GMM.\(^6\)

A model with individual effects that relaxes the time stationarity assumption is
the one we use in our estimation, where we modify the empirical model and write
the demeaned version of (1) as follows:

\[
\tilde{y}_{it} = \alpha_0 t + \sum_{j=1}^{p} \alpha_{jt} \tilde{y}_{i,t-j} + \sum_{j=1}^{p} \gamma_j \tilde{x}_{i,t-j} + \tilde{f}_i + \mu_{it} \tag{2}
\]

where \( y \) and \( x \) will be the endogenous variables we use in our specification and \( f_i \)
is the unobserved individual effect.

Before, estimating this system, we will first use a second generation unit
root test developed by Pesaran (2007) which is based on the augmentation of the
Augmented Dickey-Fuller regression with lagged cross-sectional mean and its first
difference capturing the cross-sectional dependence. We will use the critical values
reported in this paper with the null hypothesis of the presence of the unit root.\(^7\)
Moreover, we will also test the presence of cointegration for the variables having a
unit-root. If such a relationship does not exist, then we will use the first-differences
series in a Panel VAR analysis.

\(^6\) See Love and Zicchino (2006) and Arellano and Bover (1995) for details of estimation procedure.
\(^7\) We have also employed several other panel unit-root tests and obtained similar results. These are
also available upon request from the corresponding author.
Finally, once the estimation is done, we analyze impulse-response functions and also present variance decompositions. As is well known, impulse response functions aim to describe the response of an endogenous variable over time to a shock in another variable in the specified system. On the other hand, variance decompositions report the contributions of each shock to the variance of each endogenous variable, at a specified forecast horizon. Moreover, when constructing the confidence intervals of the impulse-response functions we apply bootstrap methods. Following Love and Zicchino (2006) we calculate standard errors of the impulse functions generating confidence intervals using Monte-Carlo simulations.  

4.2 Data

Motivated by Persky and Tsang (1974), we use five different variables for our empirical analysis. These are unemployment rate, unionization density, inflation rate, capital deepening and the wage-productivity gap. Ceteris paribus, we expect inflation and capital deepening to be positively and unionization to be negatively correlated with the wage-productivity gap.

Inflation data is constructed using the CPI from the International Financial Statistics. Unemployment and unionization density data are obtained from OECD Database and World Development Indicators. Capital deepening is defined as the growth rate in the aggregate capital stock. We constructed the aggregate capital stock series for each country using the perpetual inventory method using the following system of equations:

\[ K_{t+1} = K_t (1 - \delta) + I_t \]

8 Reported results are based on 1000 Monte-Carlo simulations. Results are similar when one performs different numbers of simulations.

9 In further regressions we also have experimented several other variables such as the size of the labor force, relative size of the manufacturing, growth of aggregate GDP and government spending without any qualitative change in our results. These regressions are available upon request from the corresponding author.

10 Results are similar when we construct inflation using GDP deflator from Penn World Tables.
The first equation is the standard law of motion for capital and the second one is based on the assumption that the capital-output ratio of the initial period should match the average capital-output ratio over some reference period. Here, we choose the capital stock so that the capital-output ratio in 1960 matches its average over 1951 - 1960. These two equations, along with the amount of investment, $I_t$, allows us to obtain the series of $K_t$, for all $t$. Data for investment and GDP needed to construct the series are obtained from the Penn World Tables.$^{11}$

Finally, as a measure for the wage-productivity gap we use the ratio of MPL to real wages in manufacturing.$^{12}$ The wage data come from OECD and Eurostat. To create a series for the marginal product of labor, we assume that the production in manufacturing is characterized by the following production function$^{13}$ for any year $t$ in each country $i$:

$$Y_t = A_t K_t^\alpha L_t^{1-\alpha},$$

$^{11}$The depreciation rate $\delta$ is assumed to be equal to 0.08 as standard in the Real Business Cycle literature.

$^{12}$Our choice of the manufacturing sector is necessitated by the availability of the data as wage data is only available for this sector. Noticeably, this is limiting as the other variables used in regressions are not sector-specific. However, we very much believe that estimates based on aggregate data from manufacturing are still viable due to several reasons: First, in each of the 31 countries manufacturing constitutes a significant portion of overall GDP thereby it wouldn’t be far-fetched to use ratio of aggregate wages to productivity from this sector in an analysis with aggregate unemployment, inflation, capital deepening and unionization. Second, as is evident from the labor economic literature, among other sectors, unionization is most prevalent in the manufacturing sector. That is, if any, most of the collective wage-bargaining happens in this sector. Finally, with all these features manufacturing is also the sector which is most representative for an economy in a cross-country setting. This is also why indicators from this sector is used very frequently in empirical economic literature.

$^{13}$We also replicated the same analysis with a constant elasticity of substitution production function with reasonable values for the elasticity of substitution between capital and labor calibrated to match the average capital-output ratio in the cross-sectional series and obtained qualitatively similar results.
Table 1: Complete Dataset Summary Statistics

|                         | Mean  | Std. Dev. | Minimum | Maximum | Observations |
|-------------------------|-------|-----------|---------|---------|--------------|
| Unemployment (%)        | 5.88  | 4.00      | 0.00    | 23.90   | 1229         |
| Unionization (%)        | 37.76 | 19.97     | 1.08    | 94.30   | 1232         |
| Inflation (%)           | 8.75  | 20.69     | -9.63   | 555.38  | 1345         |
| Capital Deepening (%)   | 0.38  | 2.96      | -9.42   | 25.95   | 1431         |
| Wage-Prod. Gap          | 0.87  | 0.30      | 0.45    | 2.66    | 1176         |

where $Y_t$ is the total value added (in real terms) in manufacturing, $K_t$ is the amount of capital and $L_t$ is the amount of labor used in production. In order to calculate marginal productivity of labor, $MPL = (1 - \alpha) \frac{Y_t}{L_t}$, we need an estimate of $\alpha$. Here we use hours of work in manufacturing as the measure of labor. Then, we obtain an estimate of $\alpha$, by running the following regression equation for each country $i$:

$$
\log(Y_t) = \beta_0 + \beta_1 \log(K_t) + \beta_2 \log(L_t) + \epsilon_t,
$$

where $\epsilon_t$ is the error term.

Once we have an estimate of $\alpha$, say $\hat{\alpha}$ we can easily calculate $MPL = (1 - \hat{\alpha}) \frac{Y_t}{L_t}$, and hence the MPL-to-wage ratio.

Descriptive statistics of all the variables along with the number of observations we have for each variable are provided in Table 1. We observe a significant variation for all the variables in the dataset. We have unbalanced panel data for 31 countries over the period 1960-2009. The list of countries used in the analysis is provided in the appendix.

Moreover, in Figures 1 and 2 we plot the relationship between unemployment and the wage-productivity gap in time-series and cross-section perspectives, respectively. Figure 1 reports the time-series evolution of both series as an average of all the 31 countries in the dataset. Here we observe highly fluctuating unemployment with an increasing trend over time. The wage-productivity gap series exhibits

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14 Two especially interesting observations are that the minimum unemployment rate in the data is zero and the maximum inflation rate is about 555%. The country with zero unemployment in 1961 is New Zealand. (Also see Nickel et al. (2005) for the same number. The country with inflation over 500% is Poland in 1990 right after the fall of communism.)
Figure 1: Unemployment and Wage-Productivity Gap over Time

significantly less fluctuation, however also has a slightly increasing trend over time. Moreover, in Figure 2, we observe the relationship between these two variables from a cross-country perspective. Each point in this plot represents the time-series average value of these two variables for each of the 31 countries in the dataset. From a visual perspective, Figure 2 indicates a strong positive correlation between the wage-productivity gap and the unemployment rate. Surely, one needs a proper econometric analysis to check the robustness of this plain correlation. This is what we do next in the next subsection.

4.3 Empirical Analysis

As discussed in the previous section, we first conduct a unit-root test on all the variables used in the analysis. To this end, Table 2 reports the results of the CADF
Table 2: CADF Panel Unit Root Tests

| Variable          | Level Test Stat. | Level P-value | First Diff. Test Stat. | First Diff. P-Value |
|-------------------|------------------|---------------|------------------------|---------------------|
| Unemployment      | 0.48             | 0.69          | -0.313                 | 0.00                |
| Unionization      | 1.94             | 0.97          | -3.75                  | 0.00                |
| Inflation         | 0.14             | 0.34          | -4.99                  | 0.00                |
| Capital Deepening | 1.79             | 0.89          | -5.32                  | 0.00                |
| Wage-Prod. Gap    | 0.20             | 0.42          | -3.17                  | 0.00                |

The test statistic is based on the Cross-sectionally Augmented Dickey Fuller (CADF) Test following Pesaran (2007). The test has the null hypothesis of the presence of a unit-root.

According to the results reported in Pesaran (2007), we determined the lag order in the country-specific ADF-type regressions for each series using the Akaike information criterion (AIC) model selection criterion.
Table 2, for levels of all the five variables, namely, unemployment, unionization, inflation and wage-productivity gap the null hypotheses that a unit-root is present cannot be rejected. As we reject these hypotheses for their first differences, we conclude that they are integrated of order one.\textsuperscript{17} Therefore, in our panel of 31 OECD countries, we conclude that the variables are non-stationary in their levels but stationary in first-differences.

\begin{table}[h]
\centering
\begin{tabular}{lcc}
\hline
Statistic & Value & P-value \\
\hline
$G_\tau$ & -2.28 & 0.23 \\
$G_\alpha$ & -4.10 & 0.92 \\
$P_\tau$ & -7.96 & 0.20 \\
$P_\alpha$ & -3.40 & 0.18 \\
\hline
\end{tabular}
\caption{Panel Cointegration Tests}
\end{table}

P-values are robust critical values obtained through bootstrapping with 1000 replications.

Next, in Table 3 we report the results of the cointegration test developed by Westerlund (2007). Here, we test whether a cointegrating relationship exists between the five variables we use in the analysis. Basically, our aim here is to test for the absence of cointegration which we conduct by determining whether error correction exists for the panel as a whole or for individual panel members. This test also takes using bootstrapping cross-section interdependence into account. Here the null hypothesis is that the cointegration does not exist. The $G_\tau$ and $G_\alpha$ statistics test whether cointegration exists for at least one country whereas the $P_\tau$ and $P_\alpha$ statistics pool information over all the individual country series and test whether a cointegrating relationship exists for the panel as a whole. Moreover, cross-section interdependence is taken into account by computing the robust p-value through bootstrapping with 1000 replications. According to the results in Table 3, we cannot reject the null hypothesis of no cointegration in any of the four tests.

Given the results in Tables 2 and 3 we conclude that our variables require estimation of the VAR in first differences. To this end, Table 4 reports the estimated

\textsuperscript{10} Again, we also conducted several other unit root tests and ended up with similar results.
\textsuperscript{17} We also obtained similar results using the four bootstrap tests of Smith et al. (2004).
### Table 4: Main Results of the Panel-VAR Model

| Response of | Response to | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) | Gap (-1) | Unemployment (-1) |
|-------------|-------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|----------|-------------------|
| Gap         | 1.04*       | 0.002*   |                   | (0.04)   | (0.001)           | -0.20    | 0.97*             | (0.14)   | (0.02)            |           |                   |           |                   |           |                   |           |                   |           |                   |           |                   |
| Unemployment| -0.20       | 0.97*    |                   | (0.14)   | (0.02)            | 1.04*    | 0.002*            | (0.04)   | (0.001)           | -0.08    | 0.94*             | 1.03*    | 0.006*            | (0.03)   | (0.002)           | -0.03    | 0.93*             | 0.15     | -0.06             | 0.24     | (0.08)            |
| Unemployment| -0.03       | 0.93*    | 0.004*            | (0.03)   | (0.002)           | -0.08    | 0.94*             | (0.13)   | (0.02)            | -0.03    | 0.93*             | 1.03*    | 0.006*            | (0.03)   | (0.003)           | -0.03    | 0.93*             | 0.24     | (0.10)            |
| Union       | -0.03       | 0.93*    | 0.04**            | (0.08)   | (0.03)            | -0.03    | 0.93*             | (0.08)   | (0.03)            | 1.03*    | 0.006*            | -0.03    | 0.93*             | (0.11)   | (0.03)            | -0.03    | 0.93*             | 0.24     | (0.10)            |
| Inflation   | -0.03       | 0.93*    | 0.04**            | (0.08)   | (0.03)            | -0.03    | 0.93*             | (0.08)   | (0.03)            | 1.03*    | 0.006*            | -0.03    | 0.93*             | (0.11)   | (0.03)            | -0.03    | 0.93*             | 0.24     | (0.10)            |
| Capital     | -0.005      | -0.005*  | 0.001***          | (0.003)  | (0.0007)          | 0.10     | -0.14             | (0.23)   | (0.09)            | 0.10     | -0.14             | 0.10     | -0.14             | (0.23)   | (0.09)            | 0.10     | -0.14             | 0.23     | (0.09)            |

Robust standard errors are in parentheses. *, **, *** denote 1, 5 and 10% confidence levels.
coefficients of the system. As is well known, choosing the right lag length is crucial for a robust panel VAR analysis. Given the results of the Lagrangian Multiplier test for residual autocorrelation, we choose to use one lag for each model.\(^{18}\) Moreover, we use the Cholesky decomposition when computing the impulse response functions. It is well know that ordering of the variables matters in this regard. Particularly, the variables appearing earlier are assumed to affect the other variables contemporaneously, while the ones appearing later in the VAR impact the others with some lag.

Table 5: Variance Decompositions

|       | Gap | Unemployment |
|-------|-----|--------------|
| Gap   | 0.95| 0.05         |
| Unemployment | 0.01| 0.99         |

|       | Gap | Unemployment | Union |
|-------|-----|--------------|-------|
| Gap   | 0.89| 0.08         | 0.03  |
| Unemployment | 0.01| 0.95         | 0.04  |
| Union  | 0.02| 0.05         | 0.93  |

Percent of variation in the row variable (10 periods ahead) explained by column variable.

Table 4 illustrates the estimation results of four different systems using different sets of variables in each. First, we estimate the system using only the wage-productivity gap (shortly denoted by Gap) and unemployment. Then, we add one by one unionization (shortly denoted by union), inflation and capital deepening (shortly denoted by capital) to the system. What we observe from Table 4 is that the wage-productivity gap gives a robust and significantly positive response to shocks to unemployment and negative response to shocks to unionization. Considering the fact that unemployment reduces the bargaining power of workers whereas

\(^{18}\) However, in terms of the signs of the coefficients, models with two and three lags yield qualitatively similar results.
unionization increases it, this result is not surprising. However, our empirical analysis also suggests that in the opposite direction, shocks to the wage-productivity gap do not have a significant effect on unemployment.

As discussed in Section 3, previous literature treats the wage-productivity gap as exogenous by neglecting the possible endogeneity between this gap and unemployment rate. This literature mainly tests the prediction of the theory relying on competitive markets and identifies the wage-productivity gap as a part of disequilibrium dynamics which disappears in the long-run. However, the search-theoretic models of the labor market provide a link between the aggregate unemployment rate and the wage-productivity gap, which predicts a positive correlation between these variables. Our empirical analysis provides a more flexible specification, thanks to the VAR methodology, which embeds the testing of both theoretical predictions and eliminates the potential endogeneity problems. Our empirical results indicate that the lagged values of the unemployment rate have a statistically significant effect on the wage-productivity gap. Therefore our empirical results are in line with the predictions of the search-theoretic framework.

Next, in Table 5 we present the variance decompositions for different models. In both models unemployment explains more of the wage-productivity gap variation 10 periods ahead in our sample, compared to the unionization density. However, the magnitude of the effect is rather small, unemployment explains about 5-8% of total variation in wage-productivity gap.

Finally, Figure 3 presents the impulse-response functions and the 5% error bands generated by Monte-Carlo simulations. We only report the results of the model with three variables, namely wage-productivity gap, unemployment, and unionization.

We observe from Figure 3 that the response of the wage-productivity gap is positive whereas its response to unionization is negative in the estimated coefficients and impulse responses.

5 Concluding Remarks and Discussion

In this paper, we investigate the relationship between wage-productivity gap and unemployment using a cross-country panel data set from 31 OECD countries.
spanning the period 1960-2009. A vast empirical literature analyzing the wage-productivity gap focuses on the effect of this gap on the unemployment rate which theoretically relies on the predictions of Walrasian equilibrium without any frictions in the labor market. On the other hand, labor market models which take these frictions explicitly into account and depart from the perfect competition assumption imply that the unemployment rate is a determinant of wages. Therefore, an empirical analysis which treats wage-productivity gap as exogenous may suffer from the well-known endogeneity bias. In order to avoid this bias, we exploit the dynamic panel nature of our data set and rely on the Panel-VAR estimation techniques. To the best of our knowledge, this is the first paper which employs this methodology to the research question posed in the paper.
One issue that deserves further attention is that the data we use in the paper is highly aggregate even in the macroeconomic sense. Future research should focus on the analysis of the wage-productivity gap and its relationship with different economic variables, preferably using sector, industry or firm-level data.

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Appendix

List of Countries
Australia, Austria, Belgium, Canada, Chile, Czech Republic, Denmark, Finland, France, Germany, Greece, Hungary, Iceland, Ireland, Italy, Japan, S. Korea, Luxemburg, Mexico, Netherlands, New Zealand, Norway, Poland, Portugal, Slovakia, Spain, Sweden, Switzerland, Turkey, United Kingdom, United States of America.

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