Compact Size of an Interdigital Band-Pass Filter with Flexible Bandwidth and Low Insertion-Loss Using a Folded Spiral and Stepped Impedance Resonant Structure

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Abstract: A conventional interdigital bandpass filter (BPF) is characterized by coupled and tapped lines and affords low insertion loss (IL) and easy fractional bandwidth (FBW) adjustment. However, the maximum FBW of the filter is limited to 30%, beyond that, its gap size increases, thereby rendering filter fabrication impractical on a standard printed circuit board. In addition, the filter size cannot be changed because it dictates the operational frequency of the filter. Hence, in this study, we propose a compact interdigital BPF based on a spiral and folded stepped impedance resonator (SIR), which affords low IL and excellent group delay. The spiral, folded structure facilitates drastic FBW adjustment: the center frequency and adjustable range of the FBW of the designed BPF are 800 MHz and 80 to 180%, respectively. Additionally, the proposed BPF can adjust the FBW by k-factor which can adjust from 80 to 180%. The insertion and return losses of the proposed filter are 0.043 dB and 17.1 dB, respectively, and the group delay is 0.098 ns. The total filter size is only 13.8 mm × 5.98 mm, which corresponds to a size reduction of >2/3 relative to a conventional filter and 2.1 relative to the latest BPF design. The group delay difference between the BPF and other filters is 0.15 ns. In addition, the range of adjustable FBW for the filter is 1.36 times different than for other filters.

Keywords: interdigital bandpass filter (BPF); k-factor; reduced size; stepped impedance resonator (SIR); spiral structure

1. Introduction

The demand for portable wireless communication systems is continuously increasing due to the rapid development of fourth industrial revolution technology. The requirements for a portable wireless communication system are high performance, small size, and bandwidth securing function [1]. In wireless communication, a bandpass filter (BPF) is essential. BPF should be characterized by its high performance, as well as being small and light. In order to reduce the size, a substrate with a high dielectric constant must be used. However, a substrate with a high permittivity is expensive [2]. BPF should have low loss and sufficient bandwidth to meet system specifications [2]. Therefore, many studies are being conducted to obtain a BPF that is small in size, has low loss, and with sufficient bandwidth.

Recently, the compact size of a bandpass filter has increased to 180% of bandwidth [3,4]. In this regard, microstrip BPFs offer beneficial features such as frequency selection, low insertion loss (IL) and return loss (RL), and excellent coupled−line characteristics. In particular, the high performance interdigital BPF, which affords adjustable fractional bandwidth...
(FBW) through tapped-line control at the quarter-wavelength size, is superior to BPFs with coupled structures at harmonic operating frequencies [2–8]. However, the FBW of an interdigital BPF is limited to 30% [2], and the filter size cannot be reduced easily owing to its electrical length requirement of 90° and fixed operational frequency. Some techniques are necessary for BPF designs in terms of system integration, adjustable bandwidth, and various signal processing. Here, interdigital BPFs, based on coupled structures, can be used to enhance IL, RL, and frequency characteristic performances; consequently, many studies have focused on reducing the size of interdigital filters for practical applications. Some standard interdigital filters include T-type, folded-type, and spiral-type structures [9–14]. However, BPFs based on the interdigital or other coupled-structure shapes offer limited bandwidth applications. Thus, stepped impedance resonator (SIR), balun, and multi-mode resonator (MMR) structures have also been used for adjustable bandwidth and compact BPF designs [15–22]. Specifically, the relatively large-sized SIR structures afford low IL [22,23]. BPFs with adjustable bandwidth and high performance using the bridged T-coils have also been studied; however, such filters use a metal-insulator-metal (MIM) capacitor structure, which requires additional process masking and fabrication, thereby increasing manufacturing costs [24,25].

In this article, size reduction for the interdigital BPF is presented. The proposed BPF is designed according to the SIR structure, which affords low-loss operation and adjustable bandwidth, and the resulting filter is used for λg/4 square spiral-type and λg/4 square-type SIR short stubs. The newly developed BPF is small and has low losses owing to the SIR structure. Furthermore, the filter is additionally applied to analyze the effects of the tapped line on the feeding line (k-factor), with the potential to adjust the FBW.

2. Analysis of an Interdigital Bandpass Filter

2.1. Conventional Bandpass Filter

The conventional interdigital BPF is composed of an λg/4 stub, a coupling structure, and a via hole, as shown in Figure 1 [2]; the dimensions of this BPF are a vertical length (l) of 62.6 mm, a horizontal length (WT) of 4.52 mm (4.52 mm × 62.6 mm), and the stub electrical length (θj) is 90° (λg/4).

![Figure 1. Conventional interdigital BPF layout.](image)

The coupling gap size (g1) is 0.22 mm. The FBW (Δ) of a conventional BPF can be increased by a maximum of 40%. If the coupling coefficient (M1) corresponding to the gap size (g1) increases, then the external quality factor (Qe) decreases, as given by Equations (1) and (2). Thus, the FBW increases when Qe decreases and g1 reduces, as shown in Figure 2.
Figure 2. Determination of the gap size according to (a) external quality factor and (b) coupling coefficient.

The variable \( x \) is the \( g \)-parameter of the low-pass filter prototype [2]. Table 1 shows the gap size analysis for FBW variations. The FBW of 40% corresponds to a gap size of 0.12 mm.

\[
M_{i, i+1} = \sqrt{\frac{\Delta}{x}} \quad (1)
\]

\[
Q_e = \frac{x}{\Delta} \quad (2)
\]

Table 1. Variation in FBW as a function of BPF gap size.

| \( \Delta \) [%] | 5.0% | 10% | 20% | 30% | 40% |
|-----------------|------|-----|-----|-----|-----|
| \( g_1 \) [mm]  | 0.20 | 0.18| 0.16| 0.14| 0.12|

Such an interdigital BPF is impractical because the minimum gap size needed for printed circuit board (PCB) fabrication is 0.12 mm, and this size is extremely large for practical use. Moreover, fulfilment of the size criterion is more important than optimizing the gap size because the overall size of the BPF determines its operational frequency [2,26,27].

2.2. Proposed Bandpass Filter

The proposed filter presents the possibility of adjustable bandwidth through the variation in the feeding-line position using \( k \)-factor. In addition, the designed filter has a suggested size reduction and increased performance (low insertion loss and sharp frequency cut-off). Before the introduction, the flow chart and method characteristic of the proposed filter will be explained. The flowchart (block diagram) for the proposed interdigital BPF is shown in Figure 3a. Accordingly, the BPF first involves mathematical analysis; then, the spiral and folded SIR structures are applied to the resulting short stubs, which are combined with the J-inverter. Next, the bandwidth is adjusted based on the \( k \)-factor and \( \theta_l \) to obtain the optimized BPF. The structure of the proposed BPF is introduced. The proposed size reduction in the interdigital BPF comprises \( \lambda g/4 \) square spiral-type (①: see Figure 3b) and \( \lambda g/4 \) square−type SIR (②) short stubs, as shown in Figure 3b.
Figure 3. Structure of the proposed small–sized interdigital BPF using the spiral and SIR techniques: (a) flowchart (block diagram) (b) filter structure.

In the spiral stubs (1: see Figure 3b), $Z_i$ and $Z_j$ represent the characteristic impedances, and $\theta_i$ and $\theta_j$ represent the electrical lengths of 90° each, respectively; $w_i$ and $w_j$ are the widths, and $l_{ia}, l_{ib}, l_{ic}, l_{ja}, l_{jb},$ and $l_{jc}$ are the lengths of the structure. In the square-type SIR short stubs (2:), $l_{a1}, l_{a2},$ and $l_b$ are the physical lengths; via holes of Ø 0.3 are placed at the ends of the stubs (1, 2).

The electrical length $\theta_x$ is the sum of $\theta_A$ and $\theta_B$ ($\theta_x = \theta_A + \theta_B$), corresponding to the lengths of the stubs, and is 76.5°; $\theta_x$ is defined according to Equation (3), in which the 2 is a constant [2].

$$\theta_x = \frac{\pi}{2} \left[ 1 - \frac{\Delta}{2} \right]$$  \hspace{1cm} (3)

Parameters $g_1$, $g_2$, and $g_m$ are related to the coupling gaps between the stubs and correspond to the $J$–inverter design, as shown in Figure 4. Here, parameters $I_{ij}$ and $I_{ji}$ given by Equation (4) are both 0.0044.

In Equation (4), $I_{i=A=B}$ refers to the inverter between $\theta_i$ (or $\theta_j$) and $\theta_A$ (or $\theta_B$), while $g_0, g_1,$ and $g_2$ denote the gap parameters of the resulting Chebyshev–type lowpass filter ($L_{AR} = 0.1$ dB @ symmetric structure). Thus, $g_0, g_1,$ and $g_2$ are estimated as 1.0, 1.0316, and 1.1474, respectively [2,7].

$$I_{i=A=B} = \frac{1}{Z_0} = \frac{2g_1}{g_0} \sqrt{\frac{g_2}{g_0} \cdot I_i} = I_A = B$$  \hspace{1cm} (4)
The method to adjust the bandwidth and reduce the size of the proposed BPF is shown in Figure 4. From the figure, the existing stubs are redesigned into a spiral structure (for square−type) and a folded−SIR structure. The SIR is designed with an SIR structure that can satisfy the conditions of $Z_B < Z_A$ and $Z_T = 0$. At this time, the spiral structure and the folded−SIR structure are inserted into the resonant part ($Y_i$ and $Z_A$ and $Z_B$) of the J−inverter. Then, the J−inverter (−90°) uses the coupling structure ($g_1$, $g_2$ in Figure 3b). Accordingly, the size of the BPF can be reduced with the square−type structure, while also utilizing the SIR structure [28]. Thus, the technique for producing a small size and an adjustable bandwidth forms the necessary mathematical analysis of the electrical parameters ($k$-factor). The physical performance is analyzed with the admittance inverter (J−inverter) and characteristic impedances of the short stubs with square spiral−type and square SIR−type structures, as shown in Equation (3).

![Figure 4. Equivalent circuit of the proposed BPF.](image)

To adjust the bandwidth, the BPF uses an SIR structure with open stubs. First, we need to create a resonance condition. By ignoring the discontinuous structure of the line, the impedance ($1/Z_T$) is zero ($1/Z_T = 0$), as shown in Equation (5).

$$\frac{1}{Z_T} = jZ_A \left[ \frac{2(k\tan\theta_B + \tan\theta_A)(k - \tan\theta_B\tan\theta_A)}{k(1 - \tan^2\theta_B)(1 - \tan^2\theta_A) - 2(1 + k^2)\tan\theta_B\tan\theta_A} \right] = 0 \tag{5}$$

At this time, when $Z_T = 0$ (see Figure 3b), resonance that meets the condition for impedance matching occurs. Therefore, when designing the structure of the proposed filter, in order for $Z_T = 0$, the actual structure must be $Z_B < Z_A$, and the length of $Z_A$ must be shorter than the length of $Z_B$.

In the characteristic impedance case, $k$ is the ratio of $Z_A$ to $Z_B$, where $Z_A$ and $Z_B$ are 120.5 $\Omega$ and 85.7 $\Omega$, respectively. Here, we can adjust the value of $k$ accordingly; $k = Z_A/Z_B = 1.41$; therefore, to satisfy the resonance condition, $1/Z_T$ should be zero. As the impedance ratio changes (reduces), if $k$ is greater than 1, then the FBW exceeds 160%. When $k$ is 1.3, this FBW is 180%, as shown in Figure 5. Thus, $k$ is related to increasing the FBW and decreasing the losses. When the FBW is 180% ($k = 1.3$), the $\theta_A$ and $\theta_B$ are 0.714, 25°, and 15°, respectively. If $\tan (\theta_T/2)$ is 10.8, then $\theta_T$ is 40.12°, as shown in Equation (6).

$$\theta_T = \tan^{-1}k = \frac{f_n}{f_0} \tag{6}$$

Here, $f_0$ and $f_n$ are the center frequency and nth frequency of the passband. To satisfy the resonance condition, Equation (7) must be satisfied so that $k$ is not equal to 1 but 0 (i.e., $k = \frac{Z_A}{Z_B} = \tan\theta_A\tan\theta_B @ k \neq 1$). It is possible to convert $\theta_T$ to $l_t$ and, by changing the $l_t$ value, the bandwidth can be changed while adjusting the $k$ value. In this case, $k = Z_A/Z_B$.

$$\tan\frac{\theta_T}{2} = \frac{1}{1-k} \left[ \frac{k}{\tan\theta_B + \tan\theta_A} \right] \tag{7}$$
Therefore, the ratio of the $Z_A$ value to the $Z_B$ value is 180, and the $k$ value becomes 1.3. At this time, if the $l_t$ value is changed in the lower direction with an interval of 0.05 mm, the $k$ value is changed at an interval of 0.2. Therefore, when the value of $k$ is 1.3, the bandwidth is 180%, as shown in Figure 5a. Moreover, if $k$ is 1.0, 0.7, and 0.5, the bandwidth changes to 160%, 140%, and 120%, respectively. In addition, when $k$ values are 0.3 and 0.1, the bandwidth changes to 100% and 80%, respectively. Figure 5b shows the results of changes for $S_{21}$ and $S_{11}$ corresponding to bandwidth from 80% to 180%, depending on the $k$-factor value. When the $l_t$ value of the filter is changed at 0.05 mm intervals, the bandwidth of $S_{21}$ is changed from 80% to 180%. However, with a $k$ value of 0.1 or less, the bandwidth change has a limit. Furthermore, from the $k$ value of 1.3 or higher, the bandwidth does not increase anymore and remains fixed.

The reason for this is that if the $k$ value is less than 0.1, the feeding−line of the filter reaches from point B to point A of the filter, and no further change can be made. Therefore, it is impossible to change the $l_t$ value. Moreover, if the $k$ value exceeds 1.3, the bandwidth does not increase anymore and only the transmission−zero value increases. The reason for this is that as the ratio of the impedance ($Z_A / Z_B$) is changed, the bandwidth increase function is lost, and the resonance condition ($Z_T \neq 0$) is not met.

![Figure 5. Cont.](image-url)
Figure 5. Variation in the FBW of the SIR structure in terms of (a) \( k \)-value, (b) parameter \( S_{21} \), and (c) parameter \( S_{11} \).

In relation to structural design (FBW = 180%), the characteristic impedances \( Z_{oe} \) and \( Z_{oo} \) of the even and odd modes, corresponding to the stubs and coupling structure, are expressed as Equations (8) and (9) and are estimated as 51.3 \( \Omega \) and 48.7 \( \Omega \), respectively. Consequently, \( Z_{ot} = 50 \Omega \) upon obtaining the root of the product of \( Z_{oe} \) and \( Z_{oo} \), as shown in Equation (10). At this time, the \( k_0 \) value is a variable for the change in bandwidth, and the bandwidth changes according to the change in \( k_0 \) value, and the impedance value also changes.

\[
Z_{oe} = k_0 \left[ \frac{1 + I_{i=j=A=B}}{k} + \left( \frac{I_{i=j=A=B}}{k} \right)^2 \right]
\]

(8)

\[
Z_{oo} = k_0 \left[ \frac{1 - I_{i=j=A=B}}{k} + \left( \frac{I_{i=j=A=B}}{k} \right)^2 \right]
\]

(9)

\[
Z_{ot} = \sqrt{Z_{oe}Z_{oo}} \quad [\Omega]
\]

(10)

The feed line locations for input and output can be expressed by Equations (11)–(14). Then, \( \theta_t \) and \( l_t \) denoting the physical and electrical lengths from point A to point B (Figure 3) can be estimated as 9.3\(^\circ\) and 1.07 mm (FBW: 180%), respectively [2]. Furthermore, parameters \( \lambda_g \) and \( \lambda_0 \), denoting the guided and free-space wavelengths, are estimated as 0.073 mm and 0.15 mm, respectively. Meanwhile, \( \varepsilon_r^g \) and \( \varepsilon_r^o \) are set as 4.68 and 3.76, respectively [2]. Parameters \( z \) (@ \( Z_i, Z_j, Z_A, \) and \( Z_B \)) and \( y \) denote the normalizations of the impedances and admittances, respectively, as viewed from point A (see Figure 3).

\[
\theta_t = -\tan^{-1} \left[ \frac{1}{I_{i=j=A=B}} \right] \sqrt{\frac{1 - I_{i=j=A=B}}{1 - \left( zI_{i=j=A=B} \right)^2}}
\]

(11)

\[
z = \frac{1}{1 + jytan\theta_t} \quad \text{and} \quad l_t = \frac{I_{i=j=A=B}}{1/Z_0}
\]

(12)

\[
l_t = \frac{\theta_t}{2\pi} \lambda_g \quad [\text{mm}]
\]

(13)

\[
\lambda_g = \lambda_0 \left( \sqrt{\varepsilon_r^g\varepsilon_r^o} \right)^{-1/2}
\]

(14)

The physical widths (\( g_x, x+1 \)) corresponding to \( g_1, g_2, \) and \( g_m \) can be calculated from Equations (8) and (9); they are 0.22 mm each [2]. The permittivity \( \varepsilon_r (=2.54) \) and mutual
capacitance $C$ (0.04 pF) between the stub and ground plane of the substrate are estimated using Equations (15) and (16), respectively, and the angular frequency $\omega$ ($=2\pi f_0$) is 800 MHz. The size of the complete BPF is 13.8 mm $\times$ 5.98 mm.

$$g_x = \frac{2}{\pi} \text{tanh}^{-1} \left[ \exp \left( \frac{-\pi C \cdot x + 1}{2\epsilon_r} \right) \right] \ @ x = 1 \text{ to } 2 \text{ and } x + 1 = m \tag{15}$$

$$C = \frac{\tan\theta_{ii}}{Z_0 \omega} \tag{16}$$

3. Fabrication and Experimental Results

The proposed BPF was fabricated, as shown in Figure 6a, using a low relative permittivity Teflon substrate (Taconic) with a dielectric constant of 2.54, a height of 0.54 mm, and a tangent loss ($\tan \delta$) of 0.002. We used the wet etching fabrication process with a film for negative development.

![Figure 6](image_url)

**Figure 6.** Fabrication of a new bandpass filter: (a) photograph and (b) fabrication process (wet etching).

In the fabrication process, the film is developed through development, water, fixer, and dry processes through X-ray imaging, as shown in Figure 6b, to manufacture the filter. The substrate is put on the spin-quarter, then the photo resistor (TPR) solution is applied, and then the spin operation is performed. Then, after UV-patterning of the substrate and film, the TPR solution is sacrificed using TPR development. Finally, the production of the filter is completed through wet etching.

Figure 7 shows the experimental results of the proposed BPF, from which we note that the simulation results for the IL and RL are better than 0.03 dB and 25.5 dB, respectively, with an FBW of 180% at a center frequency of 800 MHz. Additionally, the measured results
for the IL and RL are 0.043 dB and 17.1 dB, respectively, with an FBW of 180.3% at a center frequency of 804 MHz.

![Simulated and measured insertion and return losses.](image1)

Figure 7. Simulated and measured insertion and return losses.

Figure 8 shows the simulated and measured results of the group delay of the proposed BPF, which are 0.086 ns and 0.098 ns, respectively, at a center frequency of 800 MHz. In Figures 7 and 8, the simulation results were obtained using the Zeland IE3D EM simulator. At this time, EM analysis was performed by dividing the cell per wavelength of the structure by 20 (@ highest frequency: 10 GHz).

For the measurement results in Figure 7, a vector network analyzer (VNA) was used. At this time, calibration was performed. The calibration process was performed in the order of termination, i.e., open, short, load, and thru (50 Ω). Finally, to express the simulation and measurement results, the Origin Pro simulator tool was used to edit the results for clarity.

![Simulated and measured group delays of the designed BPF.](image2)

Figure 8. Simulated and measured group delays of the designed BPF.
4. Discussion

The proposed BPF exhibits FBW increment and size reduction by factors of 6 and 2/8, respectively, relative to the values of the structure in [2] (see Figure 1). The new BPF design allows an FBW increase from 80% to 180% by adjustment of the coupling ($g_i$) and $l_t$. In addition, the IL of the BPF can be controlled by adjusting $l_t$ [2]. Here, we note that, while the FBW of the conventional interdigital BPF can be sufficiently increased by adjusting $l_t$ and $s_j$ [2], it is practically limited to a maximum of 30% [2] because the maximum FBW of the $J$–inverter in the interdigital BPF is 30%. Therefore, the filter uses the SIR structure instead of a conventional resonator to increase FBW. The resonant condition of the SIR is $1/Z_T \neq 1$ because of its discontinuous structure [28]; when $1/Z_T = 1$, this resonance condition cannot be satisfied.

In general, filters with via holes are known to generate parasitic energy losses [29]; however, the newly designed BPF has low losses and a planar structure because its feed line comprises a tapped–line structure that is directly connected to the stub with a spiral structure [2]. Parallel–coupled and edge–coupled BPFs are generally composed of coupled lines between the feed lines and stubs. The coupling structure heavily depends on the electric (E)–field energy and generates dielectric losses (coupling losses). However, as noted above, the feed line of the BPF is directly connected to the stub and has low coupling loss [30,31]. Therefore, it is possible to integrate the proposed interdigital BPF with other systems. If the BPF is designed for an FBW of 180%, the resulting size increase corresponds to a decrease in $Z_B$ [32], which means that $k = 1$; thus, the resonant condition no longer holds and the operational frequency decreases. In this new BPF, the SIR characteristics are excellent, owing to the presence of an attenuation pole [32]. Table 2 shows the comparison of the proposed BPF with other filters from previous studies [33–38].

| Ref [#] | $f_0$ [GHz] | FBW [%] | IL [dB] | RL [dB] | Size [mm²] | Structure |
|---------|-------------|---------|---------|---------|------------|-----------|
| This work | 0.80 | 180 | 0.043 | 17.1 | $13.8 \times 5.98$ | interdigital BPF |
| [33] | 1.80 | 42.0 | 0.70 | 15.0 | $23.12 \times 22.76$ | stub–coupled line |
| [34] | 2.45 | 32.0 | 2.30 | 10.0 | $27.0 \times 27.0$ | SIR with DGS |
| [35] | 2.00 | 133 | 0.90 | 18.2 | $40.96 \times 12.33$ | slot–line SIR |
| [36] | 2.35 | 55.3 | — | 46.5 | $35.0$ | parallel coupled line |
| [37] | 1.80 | 55.4 | 1.00 | 11.5 | $51.5 \times 48.2$ | interdigital–SIR |
| [38] | 2.56 | 128 | 0.50 | 20.0 | $21.5 \times 10.0$ | multimode resonator |

The frequency bands in the table are applied to urban networks and LTE networks [39,40]. At this time, 800 MHz (791–821 MHz) is used in France, Germany, Italy, Morocco, and Tunisia, and 2.5–2.6 GHz and 1.8 GHz are used as LTE in Ghana, Canada, Colombia, Brazil, and south India (urban network). In particular, LTE and LTE–A are applied to 800 MHz–2600 GHz [a]. Therefore, the proposed filter is analyzed as being applicable for LTE equipment in each country.

The proposed BPF can thus be applied to mobile systems for smart factories, smart farms, and medical systems involving artificial intelligence (AI) and Internet of Things (IoT)–based applications in the fourth industrial revolution.

5. Conclusions

In this study, we used a stepped impedance resonator (SIR)–based design to fabricate a compact interdigital bandpass filter (BPF) that affords satisfactory insertion loss (IL), return loss (RL), and adjustable bandwidth performances. Conventional interdigital BPFs have a maximum fractional bandwidth (FBW) of 30%, with a size of 4.56 mm × 65.6 mm at a center frequency of 800 MHz; however, the designed BPF exhibits an FBW of 180%, with an overall size of 13.8 mm × 5.98 mm at 800 MHz. To reduce the size, we used a spiral design; moreover, the square folded SIR–type structure afforded FBW enhancement.
The proposed approach can be used to design BPFs whose impedances can be matched to the tuning parameters $l_i$ (k-factor); therefore, the BPF exhibits reduced IL and RL. In addition, the parameter $l_i$, and hence the feed line position of the BPF, can be accurately estimated. The proposed BPF is smaller than conventional filters, with a size that is approximately 2/8 times smaller than conventional filters. The designed filter size is smaller by a factor of 2.1 compared to the latest BPF filters. The group delay difference between the proposed and conventional BPFs is at least 0.15 ns, and the FBW of the proposed BPF is 1.36 times that of the latest filters.

The proposed approach also enables the design of application specific BPFs, and the planar structure ensures easy system integrability for mass semiconductor fabrication, which additionally reduces production costs. Thus, the production of such BPFs can be easily scaled to address the problem of high demand.

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