Terahertz Meets Untrusted UAV-Relaying: Minimum Secrecy Energy Efficiency Maximization via Trajectory and Communication Co-design

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January 22, 2024

Abstract

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Abstract—Unmanned aerial vehicles (UAVs) and Terahertz (THz) technology are envisioned to play paramount roles in next-generation wireless communications. In this paper, we present a novel secure UAV-assisted mobile relaying system operating at THz bands for data acquisition from multiple ground user equipments (UEs) towards a destination. We assume that the UAV-mounted relay may act, besides providing relaying services, as a potential eavesdropper called the untrusted UAV-relay (UUR). To safeguard end-to-end communications, we present a secure two-phase transmission strategy with cooperative jamming. Then, we devise an optimization framework in terms of a new measure — secrecy energy efficiency (SEE), defined as the ratio of achievable average secrecy rate to average system power consumption, which enables us to obtain the best possible security level while taking UUR’s inherent flight power limitation into account. For the sake of quality of service fairness amongst all the UEs, we aim to maximize the minimum SEE (MSEE) performance via the joint design of key system parameters, including UUR’s trajectory and velocity, communication scheduling, and network power allocation. Since the formulated problem is a mixed-integer nonconvex optimization and computationally intractable, we decouple it into four subproblems and propose alternative algorithms to solve it efficiently via greedy/sequential block successive convex approximation and non-linear fractional programming techniques. Numerical results demonstrate significant MSEE performance improvement of our designs compared to other known benchmarks.

Index Terms—UAV, THz, untrusted aerial relaying, physical layer security, minimum secrecy energy efficiency, trajectory design, resource allocation, convex optimization.

I INTRODUCTION

The unmanned aerial vehicle (UAV) has recently been recognized as one of the major technological breakthroughs to be pervasively applied in 5G-and-beyond wireless communication networks, supporting massive machine-type communications, internet of things (IoT), and artificial intelligence (AI)-empowered communications [1]–[3]. Thanks to the unique characteristics of agility, on-demand swift deployment, versatility, and channel superiority amongst the other potentialities, UAV-aided wireless communications have recently attracted a great deal of research [4]–[9]. Despite numerous advantages, the open nature of air-ground (AG) links inevitably makes such systems vulnerable to malicious attacks such as eavesdropping. Accordingly, the security and confidentiality of such promising wireless communication systems are of utmost concern and undeniable requirements. To protect the confidentiality of UAV communications against hostile entities, one promising technique is the physical layer security (PLS) that uses the characteristics of wireless channels and applies communication techniques to combat attacks without complex encryption. A number of works have found leveraging the PLS in UAV-aided communications plausibly effective [10]–[24]. For example, PLS has been exploited in a wireless-powered UAV-relay system to combat eavesdropping via maximizing secrecy rate by a joint design of UAV’s position and resource allocation [12]. Other efforts were made to maximize the average secrecy rate (ASR) via joint trajectory and communication design for UAV-standalone wireless system [13]–[15], for double-UAV with external jamming [16]–[18], and for secure UAV-relaying scenarios [19]–[21]. The majority of previous research has deemed the UAV to be a fully authorized and legitimate communication node in UAV-assisted relaying applications. However, when the UAV behaves as an untrusted relay, which is called untrusted UAV-relay (UUR), with the capability of information eavesdropping while assisting end-to-end communications (see [25], [26]), the system design becomes quite challenging and entirely different from the existing body of research.

Further, energy efficiency is another imperative need for UAV-aided communications due to UAVs’ inherent constraints on size, weight, and power (SWAP). Typically, the small-scale rotary-wing UAVs are powered via limited on-board batteries, leading to a restrictive operational lifetime, which undoubtedly impacts their overall system performance. Nonetheless, UAVs’ flight endurance, if properly designed, can be enhanced to a considerable extent [27]. Most recently, some works have studied the secrecy performance of UAV-aided systems considering the propulsion energy consumption constraint [28]–[31]. In [28], the authors have investigated ASR maximization for a cooperative dual-UAV secure data collection with propulsion energy limitation. Exploring the problem of secrecy energy efficiency (SEE) maximization for UAV-aided wireless systems is another research path [29]–[31]. The authors have designed both trajectory and resource allocation for the energy-efficient secure UAV communication system with the help of a multi-antenna UAV-jammer in [29]. Some appropriate system designs have been conducted for the SEE improvement of a single UAV-relay system [30], and a UAV-swarm multi-hop relaying scenario [31]. It is worth pointing out that all the
aforementioned designs have only aimed to combat external terrestrial eavesdroppers.

On the other hand, owing to the ultra-broad bandwidth at the terahertz (THz) frequency range (0.1–10 THz), THz transmission has been acknowledged as a promising technology capable of catering an explosive growth of user demand of higher mobile traffic for future wireless systems [32]. However, THz links incur severe path loss and high susceptibility to environmental blockage, and molecular absorption [1], [6], [33], which limit signal propagation distance and coverage range. To overcome the hindrances, one possible solution might be exploiting UAV-aided communications in THz links. Notably, in the context of THz-UAV systems, few initial research studies have thus far been conducted. The coverage probability of the UAV-THz downlink communications was analyzed in [34], while [35] has explored a similar non-security scenario with a focus on minimizing communication delay by the joint design of a UAV’s location and power control. When it comes to security issues of such high-frequency systems, despite the widely-assumed improved resiliency against eavesdropping of THz links, the authors of [36] have characterized the possibility of eavesdropping attacks for such systems. Needless to mention that even considering negligible information leakage towards the external malicious eavesdroppers through THz transmissions, the scenarios involving untrusted relays, particularly the UUR systems, may still be vulnerable to eavesdropping. The appropriate design for such systems has yet to be understood; therefore, one needs to design novel frameworks to enable the efficient deployment of THz-UUR wireless systems.

I-A Our contributions

To the best of our knowledge, this is the first work addressing the energy-efficient secure design of a THz-UUR wireless communication system to guarantee confidentiality and transmission secrecy with the least system power consumption. Our detailed contributions are summarized below.

- We present an UUR-enabled wireless communication system for data collection from multiple ground user equipments (UEs) towards the base station (BS) over THz-based AG links. We adopt a secure two-phase transmission strategy using destination-assisted cooperative jamming (DACJ) to improve security.

- Then, we formulate a maximization problem in terms of a new measure minimum secrecy energy efficiency (MSEE), defined as the minimum ratio of achievable ASR to average system power consumption. This optimization problem leads to a joint design of key system parameters, including UUR’s trajectory and velocity, communication scheduling, and network transmission power allocations.

- Since the optimization problem is originally intractable due to non-convexity, we decompose it into four subproblems and then solve each inspired by the successive convex approximation (SCA) or Dinkelbach fractional programming techniques. Further, we propose two computationally efficient algorithms according to the sequential and maximum improvement (MI) based block coordinate descent (BCD) approaches with guaranteed convergence to at least a suboptimal solution. We also thoroughly conduct computational and complexity analysis and show that our solution can be obtained in polynomial time order, making it applicable to the energy-hungry UAV-based scenarios.

- We conduct extensive simulations to verify the analyses and demonstrate the effectiveness of our proposed designs in terms of MSEE compared to some other benchmarks; i.e., without communication resource allocation design or trajectory and velocity optimization and ignoring flight power consumption. We also investigate the impact of some fundamental setting parameters such as the flight mission time, the molecular adsorption factor, the average network transmit power budget, and the flight power limit on the overall system performance.

Notation: We use bold lower case letters to denote vectors. 

\[ \| \cdot \| \] denotes Frobenius norm; \( \mathbb{E}\{x\} \) stands for the expectation over the random variable (r.v.) \( x \); \( \mathcal{CN}(\mu, \sigma^2) \) denotes a circularly symmetric complex Gaussian r.v. with mean \( \mu \) and variance \( \sigma^2 \); \( (x)^+ = \max\{x, 0\} \) and \( \max \) stands for the maximum value; \( \lfloor x \rfloor \) is the smallest integer that is larger than or equal to \( x \); \( \mathcal{O}(\cdot) \) denotes the big-O notation.

The rest of the paper is organized as follows. Section II introduces system model and formulates the problem of interest. In Section III, we present efficient iterative algorithms to solve the optimization problem, followed by numerical results and discussions given in Section IV. Finally, we draw our conclusions in Section V.

II System model and problem formulation

We consider a UAV-enabled wireless communication system for data collection from a set of \( K \) ground UEs towards a BS via a UAV-assisted mobile amplify-and-forward (AF) relay, as shown in Fig. 1. Here we assume that there are no reliable direct links from UEs to BS (see [26], [37] and references therein), and all nodes are equipped with a single antenna, operating in half-duplex mode. Therefore, a UAV-relay is employed to assist end-to-end communications [20]; nonetheless, the UAV-relay may not be fully authorized to access collected confidential information and may conduct malicious eavesdropping, i.e., a UUR [25]. Thus, secure data transmission is in demand.
Remark 1. Note that in this work, we consider a single-antenna untrusted UAV-relaying scenario focusing on the secure energy-efficient design. Extension to energy-constraint multiple-antenna UAV [9] under THz bands is intriguing but challenging, which can be investigated in future works, particularly taking into account the following factors. Firstly, the multi-input multi-output (MIMO) signal processing not only brings on higher complexity with the hardware costs due to several active elements and radio frequency (RF) chain, but also more energy consumption, which is constrained by the UAV’s SWAP limitations, and should be carefully considered in the future designs. Further, the lack of rich scattering in the UAV environment, compared to the terrestrial communication systems, considerably limits the spatial multiplexing gain of MIMO, leading to only marginal rate improvement over single-antenna UAV systems [8]. Last but not least, due to UAV’s highly dynamic environment, it would be particularly challenging to achieve transceiver beam-alignment for directional beamforming, while otherwise, beam misalignment degrades the multi-antenna diversity gain.

Without loss of generality, we consider a three-dimensional (3D) Cartesian coordinate system, where the BS’s horizontal coordinate is located at the origin \( q_0 = [0, 0] \in \mathbb{R}^{1 \times 2} \), and the ground UEs with horizontal fixed\(^1\) coordinates \( q_k = [x_k, y_k] \in \mathbb{R}^{1 \times 2} \), \( k = 1, 2, \ldots, K \), are randomly distributed in a circular annulus region with the inner radius \( R_1 \) and outer radius \( R_2 \) and the coordinates are assumed to be known in prior. Here, \( R_1 \) is considered to be the smallest distance at which a reliable uplink transmission can be obtained, while beyond \( R_1 \) in our case implies no direct link between UE and BS. Further, \( R_2 \) indicates the boundary of the permitted flying region for the UAV to provide communication service.

We also consider that UAV flies from and back to the same specific point over the region of interest for a duration of \( T \) seconds in order to provide relaying services to all UEs with fairness. This specific point may refer to the checkup point wherein the UAV gets recharged and physically examined to maintain its service. Assuming that UAV flies at a fixed altitude\(^2\) \( H \) meters whose instantaneous horizontal coordinate and velocity is represented by \( v(t) = [x(t), y(t)] \) and \( v(t) = \frac{dq(t)}{dt} \), respectively, where \( 0 < t < T \). For the ease of analysis, we adopt the time-slotted system such that the flight duration \( T \) is equally discretized into \( N \) sufficiently small time slots of duration \( T/N \). Hence, the UAV’s horizontal location at time slot \( n \) in \( N = \{1, 2, \ldots, N\} \) can be approximated by \( q[n] = [x[n], y[n]] \). This assumption is valid when \( d_{\text{max}}^\text{u} \leq \delta T/N \), wherein \( d_{\text{max}}^\text{u} \) denotes the maximum UAV’s displacement per time slot.

\(^1\)Note that in a more realistic environment all the network nodes, including terrestrial UEs, apart from the UUR, might be mobile depending on the application [38]. However, considering the high velocity and flexibility of the UAV compared to the ground nodes, we consider the ground terminals quasi-stationary throughout the flight mission with unchanged coordinates.

\(^2\)Fixed-altitude operation can be justified from a practical viewpoint in order for UAV to cut off extra energy consumption arising from ascending or descending [15], [16].

II-A Channel model

We assume that the AG links are over THz channels, which are mainly affected by both free space spreading loss and the molecular absorption according to [35]. Further, as per widely used assumption in the body of existing UAV literature, e.g., [13], [29], [39], the Doppler effect due to the UAV mobility is also considered to be perfectly compensated for ease of exposition in the sequel. Therefore, assuming that at each time slot \( n \) the channel state information is regarded static due to adequately small \( \delta T \), we adopt the line-of-sight (LoS) dominant time-varying THz channel power gain model, similar to [35], between the UUR and any UE \( k \in K \) as

\[
h_{ku}[n] = \beta_0 \exp(-a_f d_{ku}[n]) \bigg/ d_{ku}^2[n], \quad \forall n
\]

where \( d_{ku}[n] \) denotes the Euclidean distance between the UUR and the \( k \)-th UE, given by

\[
d_{ku}[n] = \sqrt{||q[n] - q_k||^2 + H^2}, \quad \forall n
\]

Note that the multiplicative term \( \exp(-a_f d_{ku}[n]) \) in (1) is the indication of excessive path loss of THz links due to water vapor molecular absorption effect\(^3\), wherein \( a_f \) is the frequency and chemical composition of air dependent adsorption factor [42]. It should be also pointed out that the main cause of absorption loss in THz frequency ranges is the water vapor molecules that cause discrete, but deterministic loss to the signals in the frequency domain. Further, \( \beta_0 \triangleq \left( \frac{C}{4\pi f} \right)^2 \) denotes the reference channel power gain at unit distance, wherein \( C \) is the speed of light, \( f \) is the operating frequency.

Likewise, the THz channel power gain between the UUR and the BS can be written as \( h_{bu}[n] = \beta_0 \exp(-a_f d_{bu}[n]) \bigg/ d_{bu}^2[n] \), where \( d_{bu}[n] = \sqrt{||q[n] - q_b||^2 + H^2}, \quad \forall n \).

II-B Constraints on user scheduling, power, UAV’s mobility

We adopt the time division multiple access (TDMA) protocol for multi-user relaying services, wherein UUR serves at most one enabled UE at \( n \)-th time slot, while the other ground UEs keep silent. Therefore, letting \( \zeta_k[n] \) be a binary user scheduling variable for UE \( k \in K \) at time slot \( n \in N \), we have the user scheduling constraints as

\[
C_1 : \quad \zeta_k[n] \in \{0, 1\}, \quad \forall k, n
\]

\[
C_2 : \quad \sum_{k \in K} \zeta_k[n] \leq 1, \quad \forall n
\]

where \( \zeta_k[n] = 1 \) if UE \( k \) is scheduled at time slot \( n \), and \( \zeta_k[n] = 0 \), otherwise. Further, the transmit powers of the UUR, the BS, and \( k \)-th user in time slot \( n \), denoted respectively as

\(^3\)It is worth stressing that THz transmissions generally admit various peculiarities such as molecular absorption effect, spectral broadening, frequency selectivity, and so forth [33], [40]. In light of this, to confront the high frequency-selectivity nature in the THz band, the total bandwidth of the THz frequencies is generally divided into several sub-bands [41]. Therefore, this work considers only one sub-band equally shared amongst communication nodes with the associated carrier frequency, and the molecular absorption effect is the solely peculiar trait we take into account in this work for ease of exposition as in [35], [41].
\( p_u[n], p_b[n], \) and \( p_k[n] \), are generally subject to average and peak transmit powers given as

\[
\begin{align*}
\text{C3:} & \quad \frac{1}{N} \sum_{n=1}^{N} \sum_{k=1}^{K} \zeta_k[n] p_k[n] \leq p^\text{ave}_k, \\
\text{C4:} & \quad 0 \leq p_k[n] \leq p^{\text{max}}_k, \quad \forall k, n \\
\text{C5:} & \quad \frac{1}{N} \sum_{n=1}^{N} p_u[n] \leq p^\text{ave}_u, \\
\text{C6:} & \quad 0 \leq p_u[n] \leq p^{\text{max}}_u, \quad \forall n \\
\text{C7:} & \quad \frac{1}{N} \sum_{n=1}^{N} p_b[n] \leq p^\text{ave}_b, \\
\text{C8:} & \quad 0 \leq p_b[n] \leq p^{\text{max}}_b, \quad \forall n
\end{align*}
\]

where \( \zeta_k[n] \) is a function of the \( k \)-th propagation factor, \( p^\text{ave}_k \) and \( p^{\text{max}}_k \) are the corresponding average and maximum power constraints of the network nodes.

The mechanical power consumption of the energy-limited UAV due to high demand of propulsion energy for aerial operation with fixed-altitude flight can be approximately given by [27]

\[
P_f[n] = P_0 \left( 1 + \frac{3\|v[n]\|^2}{2\Omega^2 R_u^4} \right) + \frac{1}{2} d_0 \rho s A_u \|v[n]\|^3 + P_i \left( 1 + \frac{\|v[n]\|^4}{4\mu_0^2} \right) + \|v[n]\|^2 \frac{v_0}{2\eta_0^2}, \quad \forall n
\]

wherein \( v[n] \) is the UAV’s instantaneous velocity at time slot \( n \), \( P_0 \) and \( P_i \) are two constants representing UAV’s \textit{blade profile power} and \textit{induced power} in hovering mode, respectively, \( \Omega_u \) and \( R_u \) are the UAV’s blade angular velocity in Radian per second (rad/s) and its rotor radius in meter (m), \( d_0, \rho, s, \) and \( A \) indicate the unit-less fuselage drag ratio, air density in kg/m^3, rotor solidity, and rotor disk area in m^2, respectively. Further, the average rotor induced velocity in hovering is shown as \( v_0 \). Thus, we have the average flight power consumption constraint as

\[
\text{C9:} \quad \frac{1}{N} \sum_{n=1}^{N} P_f[n] \leq \bar{P}_\text{lim},
\]

wherein \( \bar{P}_\text{lim} \) indicates the UAV’s average propulsion power budget, which is proportional to the UAV’s on-board battery capacity. Therefore, it should be required that the \textit{total consumed propulsion energy} by the UAV over \( N \) time slots be less than such limit in order for network functioning. Further, the considered scenario should be subject to UAV’s mobility constraints in terms of initial and final locations for cyclic path, in-flight maximum displacement per time slot for satisfying channel invariant assumption, and permitted flying region as

\[
\begin{align*}
\text{C10:} & \quad q[0] = q[N] = q_f, \\
\text{C11:} & \quad q[n+1] = q[n] + v[n] \delta_t, \quad \forall n \setminus N \\
\text{C12:} & \quad \|v[n]\| \leq v^{\text{max}}_u, \quad \forall n \\
\text{C13:} & \quad \|v[n] + 1 - v[n]\| \leq a^{\text{max}}_u, \quad \forall n \setminus N \\
\text{C14:} & \quad \|q[n] - q_f\| \leq R_2, \quad \forall n
\end{align*}
\]

where \( q_f \) indicates UAV’s initial and final location per flight, \( v^{\text{max}}_u \) and \( a^{\text{max}}_u \) are the UAV’s maximum speed and acceleration, respectively.

\[\text{II-C Secure transmission strategy, problem formulation}\]

For the purpose of wireless security, we adopt a secure two-phase transmission strategy with destination-assisted cooperative jamming (DACJ) technique similar to [13], [20], [26]. In the first phase, at each time slot \( n \), the scheduled UE \( k \) sends confidential information to UUR, and simultaneously the BS jams UUR. As such, the received signal at UUR in time slot \( n \) can be represented by

\[
x_u[n] = \sqrt{p_k[n]} h_{ku}[n] s_k[n] + \sqrt{p_b[n]} h_{bu}[n] s_b[n] + n_u[n], \quad \forall n
\]

where \( s_k[n] \) is the normalized information signal, i.e. \( \mathbb{E}(\|s_k[n]\|^2) = 1, \forall k, n \). Plus, \( s_k[n] \sim \mathcal{CN}(0,1) \) represents BS’s jamming transmission with unit power, and \( n_u[n] \sim \mathcal{CN}(0, \sigma_u^2) \) denotes the additive white Gaussian noise (AWGN) at UUR. In the second phase, UUR forwards an amplified version of the received signals using AF relaying protocol to the BS. Here we assume that the amplification process is based on the full channel state information of UE-UUR links, i.e., the exact locations of UEs are known to the UUR, thus the normalized variable-gain of AF relaying from UE \( k \) can be obtained as

\[
G_k[n] = \frac{1}{p_k[n] h_{ku}[n] \|h_{ku}[n]\|^2 + p_b[n] \|h_{bu}[n]\|^2 + N_0}, \quad \forall k, n
\]

where \( N_0 \) indicates the noise power at UUR. Accordingly, the resultant signal at the BS, after self-interference cancellation [26], can be expressed as

\[
y_u[n] = \sqrt{p_k[n]} p_u[n] h_{ku}[n] h_{bu}[n] G_k[n] s_k[n] + \sqrt{p_b[n]} p_u[n] h_{bu}[n] n_u[n] + n_u[n], \quad \forall n
\]

where \( n_u[n] \sim \mathcal{CN}(0, \sigma_u^2) \) indicates the AWGN at the BS. Under such setting, given the equally shared communication bandwidth \( B \) Hz, the achievable end-to-end instantaneous data rate in bits-per-second (bps) from the \( k \)-th UE towards the BS at time slot \( n \) is given by

\[
R^k_{b}[n] = \zeta_k[n] B \log_2 \left( 1 + \frac{p_k[n] g_{ku}[n] p_u[n] g_{bu}[n]}{p_b[n] g_{bu}[n] + p_b[n] g_{bu}[n] + 1} \right),
\]

wherein \( g_{ku}[n] \triangleq \frac{h_{ku}[n]}{N_0} \) and \( g_{bu}[n] \triangleq \frac{h_{bu}[n]}{N_0} \). Then the UUR may overhear the confidential information with an achievable wiretap secrecy rate per Hz at time slot \( n \) as

\[
R^k_{u}[n] = \zeta_k[n] B \log_2 \left( 1 + \frac{p_k[n] g_{ku}[n]}{p_b[n] g_{bu}[n] + 1} \right),
\]
\[ N_0 \doteq B \sigma_n^2 \] denotes the equal noise power at the receivers, which is assumed for simplicity of exposition.

We adopt the ASR as one of the key secrecy metrics and the ASR of \( k \)-th UE at time slot \( N \) is
\[
\bar{R}_{sec}^k = \frac{1}{N} \sum_{n=1}^{N} \left[ \frac{1}{2} (R_b^k[n] - R_n^k[n])^+ \right] \text{bps} \tag{19}
\]
wherein \((x)^+ \doteq \max \{x, 0\}\), and the ratio \(\frac{1}{2}\) is due to the fact that secure transmission is done in two phases of equal duration at each time slot. The achievable average information bits can securely be exchanged between \( k \)-th UE and BS is
\[
B_{sec}^k = \delta_k \sum_{n=1}^{N} \bar{R}_{sec}^k[n].
\]

To fully exploit the capability of aerial platforms for communication, the limited energy resource must be considered in system design. Therefore, the total energy consumption of the UAV generally consists both the communication-related energy as well as mechanical-related propulsion energy to support the UAV’s hovering and mobility. In practice, the UAV’s propulsion power consumption is much higher than those used for communication purposes such as UEs’ signal transmission, BS’s jamming, and signal processing as well as other circuitry. Hence, we approximate the network’s total power consumption by the amount that the UAV consumes for the propulsion purpose. Consequently, for the secrecy metric, we define secrecy energy efficiency (SEE) of the proposed scheme for the \( k \)-th UE as the ratio of the achievable ASR to the approximated average system power consumption as
\[
\text{SEE}^k(\zeta, Q, P) \doteq \frac{\bar{R}_{sec}^k}{\sum_{n=1}^{N} P_f[n]} \text{ bits/Joule} \tag{20}
\]
wherein the user scheduling set \( \zeta = \{ \zeta^k[n], \forall n, k \} \), UAV’s location and velocity set \( Q = \{ q[n], v[n], \forall n \} \), and network transmit power set \( P = \{ P_k = \{ p_k[n], \forall n, \forall k \}, P_a = \{ p_a[n], \forall n \}, P_b = \{ p_b[n], \forall n \} \} \) are the involving parameters.

**Remark 2.** It is worth pointing out that for later analysis we utilize the normalized metrics, i.e., the numerator and denominator of (20) are divided by \( B \) and \( P_{\text{trans}} \), respectively, to well balance numerical values of both metrics in SEE.

To design the network so as to obtain the best performance among UEs and provide a fair quality of service (QoS) to all UEs given UAV’s stringent on-board battery, we maximize the minimum SEE (MSEE) performance of the system by
\[
(P) : \max_{\zeta, Q, P} \min_{k \in K} \text{SEE}^k(\zeta, Q, P) \quad \text{s.t.} \quad C_1 - C_{14}, \tag{21}
\]

We note that the problem \((P)\) is a mixed-integer non-convex optimization problem, which is too hard to solve optimally. The non-convexity is mainly due to the non-concave objective function with respect to (w.r.t) the optimization variables, and also having the non-smoothness operator \((\cdot)^+\) and the non-convex constraints \((C_1), (C_3),\) and \((C_9)\). Indeed, the major challenge in solving \((P)\) arises from the binary user scheduling constraint \(C_1\) and the highly coupled optimization variables in the objective function in fractional form. To make it tractable, we first remove the operator \((\cdot)^+\) from the numerator of the objective function, since the value of the objective function should be non-negative at the optimal point; otherwise, one can set, e.g., \(P_k = 0, \forall k\) and get zero MSE performance without modifying the original problem. Nonetheless, having at least a differentiable objective function, the problem is still non-convex, thereby no standard approach to solve it efficiently. To remedy this issue, we first handle the binary constraint as per the approach in [43], by relaxing \(C_1\) into continuous constraint. Then, we propose some computationally efficient algorithms to iteratively solve a sequence of approximated convex subproblems by adopting several techniques such as block coordinated descent (BCD), successive convex approximation (SCA), and nonlinear fractional Dinkelbach programming, discussed below.

### III Proposed Iterative Solution

In this section, we split the problem \((P)\) into four subproblems with different blocks of variables, then solve each block by block, while keeping the other blocks unchanged. Specifically, we delve into solving the joint user scheduling and transmit power optimization subproblem to optimize \((\zeta, P_k)\), relaying and jamming power optimization subproblems to improve \(P_a\) and \(P_b\), and lastly, the joint trajectory and velocity optimization subproblem to optimize \(Q\). Then, the overall algorithms to iteratively attain the approximate solution of \((21)\) will be given.

#### III-A Joint user scheduling and transmit power optimization

First, we relax binary variables \( \zeta \) into continuous real-valued set \( \zeta = \{ \zeta_k[n], \forall k, n \} \). The relaxed version of \( \zeta \) serves, indeed, as a time sharing factor for \( k \)-th UE at time slot \( n \). Such a relaxation in general leads the objective value of the relaxed problem to be asymptotically tight upper-bounded by that of the original binary-constrained problem [43]. Next, we define the auxiliary variables \( \tilde{P}_k = \{ \tilde{p}_k[n] \doteq p_k[n] \zeta_k[n], \forall k, n \} \). By introducing a slack variable \( \psi \), the corresponding subproblem can be equivalently represented as
\[
(P1): \max_{\zeta, Q, P} \left\{ \sum_{n=1}^{N} \tilde{c}_k[n] \ln \left( 1 + \frac{C_n \tilde{p}_k[n]}{\tilde{p}_k[n] + D_{k,n} \tilde{c}_k[n]} \right) \right\} \quad \text{s.t.} \quad C_1 - C_{14}, \tag{22a}
\]

\[
\frac{1}{N} \sum_{n=1}^{N} \sum_{k=1}^{K} \tilde{p}_k[n] \leq p_{k,\text{ave}}, \tag{22b}
\]

\[
0 \leq \tilde{p}_k[n] \leq \tilde{c}_k[n] \max_{n}, \forall k, n \tag{22c}
\]

\[
\sum_{k \in K} \tilde{c}_k[n] \leq 1, \quad \forall n \tag{22d}
\]

\[
0 \leq \tilde{c}_k[n] \leq 1, \quad \forall k, n \tag{22e}
\]

\[
\sum_{n=1}^{N} \sum_{k=1}^{K} \left( \tilde{c}_k[n] - \tilde{c}_k[n] \right) \leq 0, \tag{22f}
\]
where
\[
\begin{align*}
\lambda_1 &= \frac{B}{2 \ln 2 \sum_{n=1}^N P_f[n]} \quad B_{k,n} = \frac{g_{ku}[n]}{p_b[n] g_{bu}[n] + 1} \\
C_n &= g_{bu}[n] p_{ku}[n] \quad D_{k,n} = \frac{g_{bu}(p_{ku}[n] + p_{bu}[n]) + 1}{g_{ku}[n]}
\end{align*}
\]

Note that the constraint (22a) should be met with equality at the optimal point; otherwise, the value of the objective function in problem (P1) can still be increased by increasing \( \psi \), which violates the optimality.

Lemma 1. Define the bivariant functions \( Z_1(x,y; a,b) \triangleq x \ln(1 + \frac{x y}{a + b}) \) and \( Z_2(x,y; c) \triangleq x \ln(1 + \frac{c y}{x + c y}) \) over the domain \( x, y > 0 \) with the positive constants, i.e., \( a,b,c > 0 \). Both \( Z_1 \) and \( Z_2 \) are jointly concave w.r.t the variables \( x \) and \( y \).

Additionally, the inequality below near the given point \( (x_0, y_0) \) always holds with tightness:

\[
Z_2(x, y; c) \leq x_0 (1 + \frac{y_0}{x_0}) \left(\ln (1 + \frac{y_0}{x_0} - \frac{c y_0}{x_0 + c y_0}) (x - x_0) + \frac{c x_0}{x_0 + c y_0} (y - y_0)\right) \triangleq f_1^{ab}(x, y; x_0, y_0, c),
\]

Proof. Please see Appendix A.

Using Lemma 1, it can be identified that both Terms I and II in (22a) are concave w.r.t the optimization variables \( \tilde{\zeta} \) and \( P_k \), since the summation operator preserves the convexity. The non-convexity of the left-hand-side (LHS) expression is in the form of concave-minus-concave. Then, using (23) and applying the SCA technique, we approximate the non-convex constraint with the corresponding approximate convex one at each iteration. Similar restrictive approximation can also be applied to convert (22f) into a convex constraint. Given the local point \( (P_k^{(i)}, \tilde{\zeta}_k^{(i)}) \) in the \( i \)-th iteration, we can obtain a convex reformulation of problem (P1) as follows.

\[
\begin{align*}
(P1.1) \text{ : maximize} & \quad \psi \\
\text{s.t.} & \quad \sum_{n=1}^N \tilde{\zeta}_k[n] \ln \left( 1 + \frac{C_n \tilde{p}_k[n]}{\tilde{p}_k[n] + D_{k,n} \tilde{\zeta}_k[n]} \right) \\
& \quad - f_1^{ab}(\tilde{\zeta}_k[n], \tilde{p}_k[n]; \tilde{\zeta}_{k,n}, P_k^{(i)}, B_{k,n}) \geq \frac{\psi}{\lambda_1}, \quad \forall k \\
& \quad \sum_{n=1}^N \sum_{k=1}^K \left[ (1 - 2 \tilde{z}_k^{(i)}[n]) \tilde{\zeta}_k[n] + (\tilde{\zeta}_k^{(i)}[n])^2 \right] \leq 0 \quad \text{(22b)} \\
& \quad \text{(22e)}
\end{align*}
\]

Since the reformulated problem (P1.1) is convex w.r.t. the optimization variables \( \{\psi, \tilde{\zeta}, P_k\} \), it can be solved efficiently via CVX using the interior-point method [44] commencing from a feasible point. Nonetheless, due to co-existence of constraints (22e) and (24b), attaining a feasible solution is, in general, difficult. Therefore, to embark on tackling this issue, we apply the penalty-SCA (PSCA) technique, wherein the constraint (24b) is brought into the objective function as a penalty term [45]. This initially violates the binary constraint but makes the problem feasible, enabling us to iteratively employ the SCA technique to solve the resulting convex optimization problem. To proceed, we can express (P1.1) approximately as

\[
(P1.2) \text{ : maximize} \quad \psi - \mu \eta \\
\text{s.t.} \quad (24a), (24c) \quad \sum_{n=1}^N \sum_{k=1}^K \left[ (1 - 2 \tilde{z}_k^{(i)}[n]) \tilde{\zeta}_k[n] + (\tilde{\zeta}_k^{(i)}[n])^2 \right] \leq \eta, \quad (25b)
\]

where \( \eta \) is a non-negative slack variable, and \( \mu \) is the given penalty parameter. It is worth stressing that feasible set of problem (P1.2) is larger than that of (P1); thus, the parameter \( \mu \) should initially be chosen some small non-negative value to make less focus on the binary constraint, then by gradually increasing \( \mu \) and solving the convex problem (P1.2) in an alternating manner, \( \eta \) is forced to approach zero with some accuracy, and accordingly, the approximate solution of joint user scheduling and transmit power optimization can be achieved. To this end, we can obtain the optimized value of \( P_k = \{p_{ku}[n] = \tilde{p}_{ku}[n], \forall k, n\} \). Further, once the solution of the overall algorithm is obtained, we can reconstruct the corresponding binary solution of \( \tilde{\zeta} \), according to \( \tilde{\zeta} = \{\tilde{\zeta}_k[n] = \tilde{\zeta}_k[n] + 0.5\}, \forall k, n\} \).

Remark 3. The formulated convex optimization model given in (P1.1), though being convex, cannot be directly accepted by CVX, as it does not follow the disciplined convex programming (DCP) ruleset required. Given that the relative entropy function \( E_{rel}(x, y) = x \log (\frac{x}{y}) \), \( x, y > 0 \) is convex and accepted by CVX, we can rewrite convex function \( Z_1(x,y; a,b) \) (or the equivalent expression in the constraint (22a)), as

\[
Z_1(x,y; a,b) = \frac{1}{b} \left[ (y + bx) \ln \left(1 + \frac{ay}{y + bx}\right) - \frac{1}{a} \right] \\
\cdot \left[ a y \ln \left(1 + \frac{ay}{y + bx}\right) \right] \\
= - \frac{(a + 1) y + bx, (a + 1)y + bx}{ab} \right) E_{rel}(y + bx, (a + 1)y + bx) \cdot \left(1 + \frac{ay}{y + bx}\right) \\
= - \frac{(a + 1) y + bx, (a + 1)y + bx}{ab} \right) E_{rel}(y + bx, (a + 1)y + bx) \cdot \left(1 + \frac{ay}{y + bx}\right)
\]

where the equality \((a)\) follows from the following relations between different form of logarithmic functions and the convex relative entropy function given by

\[
\begin{align*}
x \ln \left(1 + \frac{1}{y} \right) &= - E_{rel}(x, x + y), \\
x \ln \left(1 + \frac{1}{y} \right) &= E_{rel}(x + y, x + y) + E_{rel}(y, x + y)
\end{align*}
\]

where \((27)\) and \((28)\) are jointly concave and convex w.r.t the joint variables \( (x, y) \) over \( x, y > 0 \), respectively.

In terms of computational cost, for a given \( \mu \) we have \((2(NK + 1))\) optimization variables and \((K(2N + 1) + 2)\).
convex constraints in subproblem (P1.2). Assume the
convergence accuracy of SCA algorithm employed for solving
this subproblem is \( \varepsilon_1 \), the worst-case complexity of solving approximated subproblem (P1.2) can be attained as
\[ O \left( U(2NK + 1)^2(K(2N + 1) + 2)^{1.5} \log_2 \left( \frac{1}{\varepsilon_1} \right) \right), \]
where \( U \) is the maximum number of iteration required until the outer loop of the two-layer alternating optimization subproblem (P1.2) converges.

### III-B UUR’s relaying power optimization

The corresponding subproblem for optimizing UUR’s relaying power can be rewritten, introducing the slack variable \( \psi \), as
\[ (P2) : \text{maximize } \psi \]
\[ \text{s.t. } \sum_{n=1}^{N} \left[ \lambda_{k,n} \ln \left( 1 + \frac{E_{k,n}p_{u,n}[n]}{p_{u,n}[n] + F_{k,n}} \right) \right] - G_{k} \geq \psi, \forall k \]
\[ \frac{1}{N} \sum_{n=1}^{N} p_{u,n}[n] \leq p_{u}^{\text{ave}}, \quad 0 \leq p_{u,n}[n] \leq p_{u}^{\text{max}}, \forall n \]
where \( \lambda_{k,n} = \frac{B_{k,n}[n]}{2 \ln 2 \sum_{j=1}^{N} f_{j}[n]} \), \( E_{k,n} = p_{k}[n]g_{kn}[n] \) and
\[ F_{k,n} = \frac{p_{k}[n]g_{kn}[n] + p_{n}[n]g_{nu}[n] + 1}{g_{nu}[n]}, \]
\[ G_{k} = \frac{\sum_{n=1}^{N} B_{k,n}[n] \log_2 \left( 1 + \frac{p_{k}[n]g_{kn}[n]}{p_{n}[n]g_{nu}[n] + 1} \right) - 1}{2 \sum_{n=1}^{N} f_{j}[n]} \]
Note that subproblem (P2) is a convex optimization problem due to having an affine objective function and all convex constraints, following from Lemma 2 introduced below.

**Lemma 2.** Let define the function \( f_{2}(x; a, b, c, d), x \geq 0 \) with positive constant values \( a, b, c, d > 0 \) as
\[ f_{2}(x; a, b, c, d) = \ln \left( 1 + \frac{ax + b}{cx + d} \right), \]
\[ = \ln \left( 1 + \frac{a}{c} - \frac{ad - bc}{cx + d} \right), \quad (30) \]
\( f_{2}(x) \) is concave subject to the condition \( ad \geq bc \), following from the fact that the function \( \ln(1 + ax) \), \( a \geq 0, x > 0 \) is concave w.r.t \( x \), whose extended-value extension is non-decreasing and \( h(x) = - \frac{1}{x} \) is also concave; therefore, \( (f \circ g)(x) \) is concave. Note that the last equality of (30) represents the understandable reformulation of the function \( f_{2}(x; a, b, c, d) \) by the CVX optimization toolbox. We also stress that for any given point \( x_{0} \), there is a unique convex function \( f_{2}^{lb}(x; x_{0}, a, b, c, d) \) defined as
\[ f_{2}^{lb}(x; x_{0}, a, b, c, d) \triangleq \ln \left( 1 + \frac{ax_{0} + b}{cx_{0} + d} \right) + \frac{ad - bc}{cx_{0} + d} (x - x_{0}), \quad (31) \]
such that \( f_{2}^{lb}(x; x_{0}, a, b, c, d) \) serves as a global lower-bound of \( f_{2}(x) \), i.e., \( f_{2}(x) \geq f_{2}^{lb}(x; x_{0}, a, b, c, d) \) [46].

Consequently, one can solve subproblem (P2) efficiently using CVX. Here, we have \( (N + 1) \) optimization variables and \( (N + K + 1) \) convex constraints. Assuming the convergence accuracy of interior-point algorithm employed for solving this convex problem with logarithmic cone is \( \varepsilon_2 \), the complexity cost of solving subproblem (P2) can be obtained as
\[ O \left( (N + 1)^2(N + K + 1)^{1.5} \log_2 \left( \frac{1}{\varepsilon_2} \right) \right). \]

### III-C BS’s jamming power optimization

Keeping the other variables unchanged and taking the slack variable \( \psi \), the BS’s jamming power optimization subproblem is given as
\[ (P3) : \text{maximize } \psi \]
\[ \sum_{n=1}^{N} \lambda_{k,n} \left[ \ln \left( 1 + \frac{H_{k,n}}{p_{b}[n] + I_{n}} \right) - \ln \left( 1 + \frac{J_{k,n}}{p_{b}[n] + K_{n}} \right) \right] \geq \psi, \forall k \]
\[ \frac{1}{N} \sum_{n=1}^{N} p_{b}[n] \leq p_{b}^{\text{ave}}, \quad 0 \leq p_{b}[n] \leq p_{b}^{\text{max}}, \forall n \]
where \( H_{k,n} = g_{kn}[n]p_{k}[n]p_{b}[n], \) \( J_{k,n} = g_{kn}[n]g_{nu}[n]p_{b}[n], \) \( K_{n} = \frac{1}{g_{nu}[n]^2}, \) and \( I_{k,n} = p_{b}[n]g_{kn}[n]g_{nu}[n]p_{b}[n] + 1 \). Notice that subproblem (P3) is non-convex due to non-convex constraint (32b), which is in the form of convex-minus-convex according to [17, Lemma 1]. Therefore, we apply SCA such that for a given local point \( F_{k}^{(l)} \) in \( l \)-th iteration. We approximate the first convex term with the global underestimator concave expression and obtain the convex reformulation as
\[ (P3.1) : \text{maximize } \psi \]
\[ \sum_{n=1}^{N} \lambda_{k,n} \left[ f_{3}(p_{b}[n]; p_{b}[n], H_{k,n}, I_{k,n}) - \ln \left( 1 + \frac{J_{k,n}}{p_{b}[n] + K_{n}} \right) \right] \geq \psi, \forall k \]
\[ (32c) \text{ & (32d) } \]
\[ \text{wherein} \]
\[ f_{3}(p_{b}[n]; p_{b}[n], H_{k,n}, I_{k,n}) = \ln \left( 1 + \frac{H_{k,n}}{p_{b}[n] + I_{k,n}} \right) - \frac{H_{k,n}}{(p_{b}[n] + I_{k,n})(p_{b}[n] + H_{k,n} + I_{k,n})} (p_{b}[n] - p_{b}^{(l)}[n]). \]

Since subproblem (P3.1) is convex, we can solve it efficiently using CVX. Here, we have \( N + 1 \) optimization variables and \( (N + K + 1) \) convex constraints. Assuming the accuracy of SCA algorithm for solving this problem is \( \varepsilon_3 \), the complexity of solving approximated subproblem (P3.1) can, therefore, be represented as
\[ O \left( (N + 1)^2(N + K + 1)^{1.5} \log_2 \left( \frac{1}{\varepsilon_3} \right) \right). \]
III-D Joint trajectory and velocity optimization

Now, we optimize the trajectory \( q \) and velocity \( v \) of the UUR while keeping the transmit power allocation and user scheduling sets \((P, \zeta)\) fixed. Therefore, the corresponding subproblem can be given as

\[
\text{(P4)} : \max_{Q} \min_{k \in K} \frac{\bar{R}_{\sec}^k(q, v)}{P_f(v)} \quad \text{s.t.} \quad C9 - C14
\]

wherein \( \bar{P}_f(v) = \frac{1}{N} \sum_{n=1}^{N} P_f^h[n] \). In order to solve subproblem (P4), we should maximize every single fractional terms of \( \left\{ \frac{\bar{R}_{\sec}^k(q, v)}{P_f(v)} \right\}, \forall k \) subject to the given constraint (35b). In light of this, let \( \lambda^* \) be the maximum MSEE of subproblem (P4) with solution set \((q^*, v^*)\) given by

\[
\lambda^* = \max_{q, v \in \mathcal{F}, k \in K} \frac{\bar{R}_{\sec}^k(q, v)}{P_f(v)} = \min_{k \in K} \frac{\bar{R}_{\sec}^k(q^*, v^*)}{P_f(v)},
\]

wherein \( \mathcal{F} \) represents the feasible set spanned by the constraint (35b). Applying nonlinear fractional Dinkelbach programming theory \([47]\), the objective function of problem (P4) can be equivalently transformed into a subtractive version such that the optimal value of \( \lambda^* \) can be achieved iff

\[
\max_{q, v \in \mathcal{F}, k \in K} \min_{k \in K} \bar{R}_{\sec}^k(q, v) - \lambda^* \bar{P}_f(v) = \min_{k \in K} \bar{R}_{\sec}^k(q^*, v^*) - \lambda^* \bar{P}_f(v^*) = 0,
\]

Thus, we can optimize the equivalent problem to obtain the optimal solution of \( Q \), via solving the reformulated problem as

\[
\text{(P4.1)} : \max_{q, v \in \mathcal{F}} \min_{k \in K} \bar{R}_{\sec}^k(q, v) - \lambda^{(m)} \bar{P}_f(v) \quad \text{s.t.} \quad (35b)
\]

wherein \( \lambda^{(m)} = \min_{k \in K} \frac{\bar{R}_{\sec}^k(q^{(m)}, v^{(m)})}{P_f(v^{(m)})} \) showing the value of \( \lambda \) in the \( m \)-th iteration of the Dinkelbach algorithm. Reformulated problem (P4.1) is still non-convex due to non-convex objective function and constraint (C9) which can be dealt with as follows.

By introducing the slack variables \( \psi \) and \( \mu = \{\mu[n]\}_{n=1}^{N} \) such that

\[
\mu[n] = \left( \sqrt{1 + \frac{\|v[n]\|^2}{4\psi^2 v^2}} - \frac{\|v[n]\|^2}{2\psi^2} \right)^{\frac{1}{2}}, \quad \forall n
\]

we can relax the problem (P4.1) to the one with the approximately equivalent but enjoying concave objective function as

\[
\text{(P4.2)} : \max_{\psi, \mu, q, v} \psi - \lambda^{(m)} \omega \quad \text{s.t.} \quad (40b), (40c), (40d)
\]

\[
B = \frac{2N \ln 2}{\beta_0} \sum_{n=1}^{N} \frac{\gamma_k}{\|q[n] - q_k\|^2 + H^2} \times \exp(a_f \sqrt{\|q[n] - q_k\|^2 + H^2}) \geq s_k[n], \quad \forall k, n
\]

\[
\frac{N_0}{\beta_0} \left( \|q[n] - q_k\|^2 + H^2 \right) \times \exp(a_f \sqrt{\|q[n] - q_k\|^2 + H^2}) \leq w[n], \quad \forall n
\]

where in (43c), we have defined \( k_0 = \frac{p[n]}{P_{\mu}[n] + P_{\mu}[n]}, k_1 = \frac{p[n]}{P_{\mu}[n] k_2 = p_k[n], k_3 = p_b[n], \epsilon = 1/(p_k[n] P_{\mu}[n] g_{\mu}[n] g_{\mu}[n]). \)

Note that all the inequality constraints (43d), (43e), and (43f) must also be met with equality at the optimal point, otherwise the optimality is violated. Following the high-SNR approximation, we set \( \epsilon \approx 0 \) in the subsequent sections for the ease of expositions. We remark the fruitful lemma below.
Lemma 3. Let define the bivariate functions \( f_{41}(x, y; a, b) \) and \( f_{42}(x, y; c, d) \), and univariate functions \( f_{43}(x; c) \) and \( f_{44}(x; c) \) with positive constants \( a, b, c, d, p, r > 0 \) as
\[
\begin{align*}
 f_{41}(x, y; a, b) &= \ln \left( 1 + \frac{1}{ax+by} \right), \\
 f_{43}(x; p) &= x^2 \exp(px), \\
 f_{42}(x, y; c, d) &= \ln \left( 1 + cx^{-1} + dy^{-1} \right), \\
 f_{44}(x; r) &= \ln \left( 1 + \frac{r}{x} \right).
\end{align*}
\]

We have the following tight inequalities
\[
\begin{align*}
 f_{41}(x, y) &\geq f_{41}(x_0, y_0) - \frac{a(x-x_0)}{a x_0 + b y_0 + 1} \triangleq f_{41}^b(x, y; x_0, y_0, a, b), \\
 f_{42}(x, y) &\geq f_{42}(x_0, y_0) - \frac{c y_0 - c y_0}{c y_0 + d x_0 + x_0} \triangleq f_{42}^b(x, y; x_0, y_0, c, d), \\
 f_{43}(x) &\geq f_{43}(x_0) + x_0 \exp(p x_0 + 2)(x - x_0) \triangleq f_{43}^b(x; x_0, p), \\
 f_{44}(x) &\geq f_{44}(x_0) - \frac{r(x-x_0)}{x_0(x+r)} \triangleq f_{44}^b(x; x_0, r),
\end{align*}
\]

Proof. Please see Appendix B.

Algorithm 1: Proposed Dinkelbach-based algorithm to approximately solve subproblem (P4)

Result: \( \mathbf{q}^*, \mathbf{v}^* \)

Initialize feasible point \((\mathbf{q}^{(0)}, \mathbf{v}^{(0)})\) and slack variables, set iteration index \( m = 0 \), then\[ \psi^{(m)} = R_{\text{sec}}^{\mathbf{q}}(\mathbf{q}^{(m)}, \mathbf{v}^{(m)}), \]
\[ \psi^{(m)} = P_{\mathbf{f}}(\psi^{(m)}), \]
\[ \lambda^{(m)} = \Delta \psi^{(m)}, \]
and set Convergence = false;

while not Convergence do

Given \((\lambda^{(m)}, \mathbf{q}^{(m)}, \mathbf{v}^{(m)})\), solve (P4.5) using (49a), then obtain \((\psi^{(m+1)}, \omega^{(m+1)}, \mathbf{q}^{(m+1)}, \mathbf{v}^{(m+1)})\);

Calculate \(\lambda^{(m+1)}\), then \(F = \psi^{(m)} - \lambda^{(m+1)}\omega^{(m)}\);

if \(|F| \leq \epsilon_2\) then

\[ \mathbf{q}^* = \mathbf{q}^{(m+1)}, \mathbf{v}^* = \mathbf{v}^{(m+1)}; \]

Convergence = true;

end

\( m \leftarrow m + 1; \)

end

wherein \(\{\mathbf{q}^{(m)}\}_{n=1}^N\) is the local given point set of optimization variables \(\mathbf{q}\) in the \(m\)-th iteration. Since subproblem (P4.5) is convex; therefore, it can be efficiently solved via CVX. It is worth noting that to solve subproblem (P4.5), we have \((3N(K + 2) + 1)\) optimization variables and \((3NK + 7N + K + 1)\) convex constraints. Assuming the accuracy of the SCA algorithm for solving this problem is \(\varepsilon_4\), the complexity of solving approximated subproblem (P4.5) for given \(\lambda^{(m)}\) can, therefore, be obtained as \(O \left( (3N(K + 2) + 1)^2(3NK + 7N + K + 1) 1.5 \log_2 \left( \frac{1}{\varepsilon_4} \right) \right)\).

Remark 4. Note that constraints given by (43e) and (43f), being in the form of \(a||x - x_0||^2 \exp(b||x - x_0||) \geq y, \) plus, the expression \(E = \ln(1 + cx^{-1} + dy^{-1})\) used in (48c) are proved to be convex; however, they indeed violate the DCP rule-set of the CVX, and so cannot be applied in the optimization model. The former can be handled by rewriting it as
\[
t_1 \geq ||x - x_0||^2, \quad t_2 + a^{-1}E_{\text{rel}}(at_1, y) \leq 0, \quad t_2 \geq b/t_1^2,
\]

And the latter can be dealt with properly by replacing \(E\)-form function appeared in (48c) with \(t_5\) and adding the constraints
\[
\frac{x}{c} \geq \exp(-t_3), \quad \frac{y}{d} \geq \exp(-t_4), \quad t_5 \geq \text{LSE}(0, t_3, t_4),
\]
wherein \(t_1 \rightarrow t_5\) are some non-zero slack variables, and the log-sum-exp function, which is a CVX-approved convex function, defined as \(\text{LSE}(x_1, x_2, \cdots, x_n) = \ln(\sum_{i=1}^N \exp(x_i))\).

III-E Overall algorithms and complexity discussion

Having obtained an efficient optimization model for each subproblem in the previous section, we are now ready to propose iterative algorithms based on sequential block optimization and maximum improvement (MI) or the so-called greedy optimization introduced in [48], summarized in Algorithm 2 and Algorithm 3, respectively. The former is simpler to implement and requires less computations at each iteration. The latter converges faster thanks to a large step-size at
Algorithm 2: Overall sequential based proposed iterative algorithm for MSEE maximization (MSEE-Seq)

1: Initialize a feasible point \((q_l, v^l, P^l_k, P^l_u, P^l_b, \zeta^l, \xi^l)\), and let iteration index \(l = 0\);
2: Repeat:
3: Solve (P1.1) using (24), updating \(P^{l+1}_k\) and \(\zeta^{l+1}\); \(l \leftarrow l + 1\);
4: Given \((P^{l+1}_k, \zeta^{l+1})\), solve (P2) using (29a), updating \(P^{l+1}_u\); \(l \leftarrow l + 1\);
5: Given \((P^{l+1}_k, \zeta^{l+1}, P^{l+1}_u, P^{l+1}_b)\), solve (P3.1) using (33a), updating \(P^{l+1}_b\); \(l \leftarrow l + 1\);
6: Given \((P^{l+1}_k, \zeta^{l+1}, P^{l+1}_u, P^{l+1}_b)\), run Algorithm 1 with \(q^{(l)}\) and \(v^{(l)}\), updating \(q^{(l+1)} \leftarrow q^*\) and \(v^{(l+1)} \leftarrow v^*\); \(l \leftarrow l + 1\);
7: Until fractional increase of objective function in (21) gets below the threshold \(\epsilon_l\);
8: Return: \((Q_{\text{opt}}, P_{\text{opt}}^{\text{opt}}, \zeta_{\text{opt}}^{\text{opt}}) \leftarrow (Q^{(l)}, P^{(l)}, \zeta^{(l)})\);

Algorithm 3: Overall greedy based proposed iterative algorithm for MSEE maximization (MSEE-MI)

1: Initialize a feasible point \((q_l, v^l, P^l_k, P^l_u, P^l_b, \zeta^l, \xi^l)\), and let iteration index \(l = 0\);
2: Repeat:
3: Do in parallel
4: 3.1: Solve (P1.1) using (24) with \((P^{(l)}_k, \zeta^{(l)})\);
5: 3.2: Solve (P2) using (29a) with \(P^{(l)}_u\);
6: 3.3: Solve (P3.1) using (33a) with \(P^{(l)}_b\);
7: 3.4: Run Algorithm 1 with \((q^{(l)}, v^{(l)})\);
8: End
9: Update one of the blocks \((P^{(l+1)}_k, \zeta^{(l+1)}, P^{(l+1)}_u, P^{(l+1)}_b)\) whose maximum improvement of objective function given in (21) gets the highest, and keep the remained blocks unchanged;
10: \(l \leftarrow l + 1\);
11: Until fractional increase of objective function in (21) gets below the threshold \(\epsilon_l\);
12: Return: \((Q_{\text{opt}}, P_{\text{opt}}^{\text{opt}}, \zeta_{\text{opt}}^{\text{opt}}) \leftarrow (Q^{(l)}, P^{(l)}, \zeta^{(l)})\);

each iteration and implementation via parallel computation capability; otherwise, it may be too expensive.

It can be mathematically proved that both algorithms are guaranteed to converge to at least a suboptimal solution. Particularly, for convergence analysis of Algorithm 2, let define the objective values of the original problem \((P)\), the subproblems \((P2)\) and \((P3.1)\) at iteration \(l\) as \(\text{MSEE} (\zeta^l, P^l_k, P^l_u, P^l_b, Q^l)\), \(\Theta (\zeta^l, P^l_k, P^l_u, P^l_b, Q^l)\), and \(\Xi (\zeta^l, P^l_k, P^l_u, P^l_b, Q^l)\). Now, we can proceed as

\[
\text{MSEE} (\zeta^l, P^l_k, P^l_u, P^l_b, Q^l) \\
\leq \text{MSEE} (\zeta^{l+1}, P^{l+1}_k, P^{l+1}_u, P^{l+1}_b, Q^{l+1})
\]

where (a) follows from the definition of the optimal solution to the optimization subproblems (P1.2). Besides, the equalities (b) and (d) hold on the grounds that the first order Taylor approximation is adopted via the SCA technique and that the objective function of (P2) and (P3.1) share the same value with the original function at the given point. Furthermore, (c) and (e) hold since the objective value of (P2) and (P3.1) are tight lower-bound to that of the original problem. Finally, (f) follows from Algorithm 1 whose convergence has been well understood [47]. From the last inequality in (52), it can be concluded that Algorithm 2 is guaranteed to converge, since the feasible solution set of \((P)\) is compact and its objective value is non-decreasing over iteration index \(l\) and that the optimal value of MSEE is upper bounded by a finite value from the communications engineering perspective. Convergence proof for Algorithm 3 follows the similar approach and hence omitted for brevity. In terms of computational complexity, given \(L\) and \(M\) be the maximum convergence iteration of the outer overall BCD-SCA algorithm and the inner fractional sub-algorithm, and based on the convergence analysis of each subproblem given in the previous subsections, Algorithms 2 and 3 have the overall worst-case complexity of approximately

\[
O \left( L(NK)^{3.5} \left( U \log_2 \left( \frac{1}{\delta_l} \right) + M \log_2 \left( \frac{1}{\delta_l} \right) \right) + LN^{3.5} \log_2 \left( \frac{1}{\delta_l^2} \right) \right)
\]

and

\[
O \left( L(NK)^{3.5} \max \left( U \log_2 \left( \frac{1}{\delta_l} \right), M \log_2 \left( \frac{1}{\delta_l} \right) \right) \right)
\]

respectively. Both are in polynomial time order and applicable to the energy-hungry UUR scenarios.

IV Numerical results and discussion

In this section, we provide some numerical simulations to evaluate the secrecy performance of the considered Thz-UUR scheme, and demonstrate the effectiveness of our proposed designs in comparison with some benchmarks. Unless otherwise stated, all simulation parameters, adopted from the literature, are given in Table I.

Since the initial feasible point is important to use the proposed BCD-SCA-Dinkelbach based algorithms and significantly impacts their convergence performance, we explain how we can obtain an initial feasible UAV’s trajectory and velocity, network transmission powers, and user schedulings. The initial UAV’s trajectory is assumed to be a circular path centered at the BS’s location with radius \(R_u = ||q_b - q_l||\),
provided that UAV’s instantaneous velocity constraint C12 is satisfied, and \( T \geq T_{\text{min}} \) is the minimum required time for circular trajectory. However, if \( T_{\text{min}} > T \geq T_{\text{min}} \), i.e., at least cyclic trajectory was possible with minimum required time \( T_{\text{min}} \), then one could use any cyclic shape as long as C10 – C14 are satisfied. Here, we consider a Piriform trajectory with discretized equations given by \( q = [x; y] \) with \( x = A_y(1 - \sin(t)) \cos(t) \) and \( x_0 = R_u(\sin(t) + 1/2) \) in which \( t_{1xN} \) indicates the linearly spaced vector in \( \left[ \frac{\pi}{2}, \frac{3\pi}{2} \right] \). Further, the constant \( A_y \) can be obtained efficiently via a simple 1D search in the range of \([R_u, 0]\) or simply set to zero. The UAV’s initial velocity vector \( v \) is then followed by \( v[n] = \frac{q[n+1]}{\delta t}, \forall n \in N \) and \( v[N] = v[N-1] \).

Having obtained an initial feasible UAV’s path planning \((Q^f = \{q; v\})\), we can set the initial UUR’s relaying power and the BS’s jamming transmission power as \( P_u = \{p_u[n] = p_u^{\text{ave}}, \forall n\} \) and \( P_b = \{p_b[n] = p_b^{\text{ave}}, \forall n\} \), respectively. The UEs’ initial transmit powers are set as

\[
P_k^i = \begin{cases} p_k^{\text{ave}}, & \text{if } \zeta_k[n] = 1, \\ 0, & \text{if } \zeta_k[n] = 0, \forall k, n \end{cases}
\]

and the UEs are scheduled equally (e.g., \( \frac{N}{K} \) times each), i.e., \( \zeta \) is obtained such that the constraint C1 holds.

After identifying the initial feasible point for the iterative optimization algorithms, we consider different benchmark schemes, all of which are detailed below and labelled in the following figures, to demonstrate the superiority of our proposed MSEE-based optimization algorithms.

- **MSEE-Seq**: Minimum Secrecy Energy Efficiency optimization scheme using the Sequential BCD-based subproblem maximization as given in Algorithm 2.
- **MSEE-MI**: Minimum SEE optimization scheme based on the Maximum Improvement subproblem maximization as given in Algorithm 3.
- **MSEE-FTrj**: Minimum SEE design with Fixed Trajectory and velocity, i.e., \( Q = \{q[n], v[n], \forall n\} \) based Minimum SEE optimization scheme using the MI-BCD approach via jointly optimizing the transmit power allocations and user scheduling, i.e., \( P_k, P_u, P_b, \) and \( \zeta \).
- **MSEE-FPow**: Jointly designing the trajectory and velocity of the UUR for the Minimum SEE design via solving the corresponding subproblem, i.e., optimizing \( Q \), while keeping the power allocations and user scheduling parameters fixed, i.e., setting them equal to the initial feasible values.
- **MASR-Seq**: Optimizing Minimum ASR given in (18) while ignoring the UUR’s flight power limit using the Sequential BCD approach to iteratively improve \( Q, P, \zeta \).

Fig. 2 depicts the convergence of the proposed iterative algorithms for \( T = 100 \) s. We can see that both benchmark schemes **MSEE-FTrj** and **MSEE-FPow** converge quickly; however, they both can achieve significantly lower MSEE performance than the proposed joint design of trajectory, power control and user scheduling schemes, i.e., **MSEE-MI** and **MSEE-Seq**. Specifically, **MSEE-MI** not only converges relatively faster than **MSEE-Seq**, i.e., 12 against 29 iterations, but offers slightly higher MSEE than that of its counterpart, as well. However, they achieve approximately 52.1% MSEE improvement, while **MSEE-FPow** and **MSEE-FTrj** can only increase the MSEE by 19.7% and 10.6%, respectively.

Fig. 3 illustrates UUR’s trajectories according to different optimization schemes with different mission duration \( T = \{7, 10, 20\} \) s. We note that when the initial circular trajectory is impossible due to significantly low mission time, e.g., \( T = 7 \) s, and owing to the UAV’s physical system limitations, the crucial task of path-planning can be efficiently designed based on the proposed MSEE-based optimization algorithms.

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**TABLE I: System parameters**

| Simulation parameter (notation) | Value |
|--------------------------------|-------|
| Gaussian noise power spectral density \( \sigma_n^2, \sigma_u^2 \) | -196 dBm/Hz |
| Operating frequency \( f \) | 0.8 THz |
| Bandwidth \( (B) \) | 10 GHz |
| Reference channel power gain \( (\beta_0) \) | -71 dB |
| Molecular absorption coefficient \( (\sigma_0) \) | 0.005 |
| UEs’ average transmission power \( (p_u^{\text{ave}}, \forall k) \) | 20 dBm |
| UEs’ peak transmission power \( (p_u^{\text{max}}) \) | 0.4 W |
| UUR’s average relaying power \( (p_b^{\text{ave}}) \) | 0.4 W |
| UUR’s peak relaying power \( (p_b^{\text{max}}, \forall k) \) | 1.6 W |
| BS’s average jamming power \( (p_b^{\text{ave}}) \) | 0.5 W |
| BS’s peak jamming power \( (p_b^{\text{max}}, \forall k) \) | 2 W |
| UUR’s operational altitude \( (H) \) | 10 m |
| UUR’s initial/terminal 2D location per flight \( (q_1) \) | [25 m, 0 m] |
| BS’s horizontal location \( (q_0) \) | [0 m, 0 m] |
| Inner and outer radii of the region \( (R_1, R_2) \) | (20 m, 30 m) |
| Number of randomly distributed UEs \( (K) \) | 5 |
| Average flight power consumption budget \( (P_{l,m}) \) | 200 W |
| UAV’s maximum velocity \( (v_{\text{max}}) \) | 5 m/s |
| UAV’s maximum acceleration \( (a_{\text{max}}) \) | 5 m/s² |
| Blade angular velocity \( (\omega) \) | 300 rad s⁻¹ |
| Rotor radius \( (r) \) | 0.4 m |
| Air density \( (\rho) \) | 1.225 kg m⁻³ |
| Rotor solidity factor \( (s) \) | 0.05 |
| Rotor disk area \( (A) \) | 0.503 m² |
| Average hovering induced rotor velocity \( (v_0) \) | 4.03 m/s |
| Fuselage drag ratio \( (d_d) \) | 0.6 |
| Profile drag coefficient \( (\delta) \) | 0.012 |
| Incremental correction coefficient of induced power \( (k_i) \) | 0.1 |
| UAV’s weight \( (W_1) \) | 20 Kg m⁻² |
| Blade profile constant \( (P_0) \) | 79.856 W |
| Parasite component constant \( (P_1) \) | 1 + 4k_i W_1 m⁻² |
| Mission time \( (T) \) | 10 s |
| Time slot duration \( (t_{\text{slot}}) \) | 0.1 s |
| Overall iterative algorithm’s convergence tolerance \( (\epsilon_1) \) | 10⁻³ |
| Convergence tolerance of Dinkelbach’s programming \( (\epsilon_2) \) | 10⁻⁴ |
on a Piriform trajectory initialization as shown in Fig. 3(a).
However, when $T$ is sufficiently high, e.g., $T = 10$ s or
$T = 20$ s, the baseline trajectory of circular shape can be
utilized. It should be mentioned that the curve belonging to the
\textit{MSEE-FTtrj} does represent the initial feasible cyclic trajectory
based on the circular or Piriform shapes, and the other curves
illustrate the optimized UUR’s trajectory according to the
different algorithms. It can be observed that the optimized
trajectories are much more complicated than the initial ones,
particularly when the UUR enjoys relatively higher mission
time and flexibility, i.e., $T = 20$ s, as shown in Fig. 3(c).

Notice that UUR should fly towards UEs’ locations to obtain
data with low power. This, in turn, can significantly increase
the chance of information leakage due to a stronger wiretap
link and less effective BS’s jamming. Thus, UUR prefers
to stay not too far from the BS. Overall, we see that the
path planning makes UUR adjust trajectory through the best
possible path, efficiently forming the distances between the
UUR, selected UEs, and the BS such that a balanced trade-
off between the channel conditions for the friendly jamming
transmission in the first phase as well as the aerial relaying in
the second phase of transmission improves the overall energy-
efficient secrecy performance. Further, we observe from Fig.
3(b) that the MSEE-based trajectories are generally smoother
than that of the \textit{MASR-Seq}, wherein the UUR prefers to
quickly reach the best locations providing service for the
designated UEs while hovering. This observation implies that
the MSEE optimization demands such smooth paths for a
lower flight power consumption of the UUR, in contrast to
the \textit{MASR-Seq} design where the UUR’s velocity might harshly
fluctuate for the minimum ASR (MASR) improvement if
required.

Fig. 4 illustrates the MASR and the average flight power
consumption (AFPC) against iteration indices for different
schemes. It is crystal clear that for the MSEE-based algo-
rithms, the MASR and the AFPC performances tend to be
non-decreasing and non-increasing, respectively. In contrast,
for \textit{MASR-Seq} scheme, the AFPC first decreases down to
some level then increases until convergence in 36 iterations.
We also note that this scheme can achieve slightly higher
MASR performance than our proposed schemes but at the
cost of significantly higher AFPC, resulting in lower MSEE
(43.13 Mbits/Joule). This reinforces the significance of energy-
efficient secure UAV-system design, which conventional works
have somewhat ignored.

Fig. 5 is plotted to demonstrate how the UAV’s velocity
(Vel.) and the instantaneous flight power consumption (IFPC)
are adjusted over time based on different algorithms. The
curves labeled with “\textit{MSEE-FTtrj}” basically represent the initial
UAV’s velocity and IFPC for all the other scenarios. We
observe that all the trajectory optimization schemes make UAV
fly with roughly less speed variation for a relatively more
extended period of time (e.g., from 2s to 10s) to satisfy mission requirements as well as improve the MSEE performance. Specifically, UUR starts at a high initial speed to fast reach the targeted location while gradually decreasing the speed down to some appropriate level, maintaining comparatively unchanged afterward for the sake of efficient power consumption purposes. Nonetheless, based on the MASR-Seq scheme, the velocity tends to be minimal while confidential relaying towards the scheduled UE; however, it changes drastically, enabling the mission to be accomplished by the end of the specified time. As it can be seen, this approach consumes relatively high flight power.

Fig. 6 illustrates the joint power allocation and user scheduling vs. time for different MSEE optimization algorithms. The sub-figure 6(d) represents the non-optimal but feasible power allocations and user scheduling adopted for initialization of all the schemes. Initially, UUR is very close to UE_{5} but far from the BS. Hence, UE_{5} is scheduled due to a possibly better channel condition than the others, and the BS jams in high power while UE_{5} keeps low power. For MSEE-FTrj, UUR follows the circular trajectory while maintaining the same distance from the BS that has a constant jamming power. In contrast, sub-figures 6(a), 6(b), and 6(e) show that at initial stage, UE_{5} increases power when UUR heads towards the BS and the BS reduces jamming power. Further, these UEs are scheduled unequally, but during their scheduling, except UE_{5}, they need to utilize their maximum transmission powers for sending information, and the relaying power slightly fluctuates around $p_{u}^{\text{ave}}$.

Fig. 7 depicts how the MSEE performance varies when the molecular absorption coefficient of THz links changes from $\alpha_f = 0.005$ to $\alpha_f = 0.025$ (similar range is also adopted in [35]), which can be physically translated to different carrier frequencies and environmental effects. From the figure, we can see that the larger the molecular absorption coefficient, the lower the MSEE performance for all the schemes due to higher propagation loss arising from severe molecular absorption. It is worth pointing out that the increased propagation loss results in the reduction of not only UUR’s information leakage, but also BS’s reception quality. Nonetheless, our proposed MSEE-MI and MSEE-Seq schemes substantially outperform the others regardless of the environmental conditions and operational carrier frequency of THz links.

In Fig. 8, we investigate how the mission time $T$ impacts the MSEE performance for different schemes. Evidently, for the fixed trajectory schemes, i.e., MSEE-FTrj and the non-optimal initial feasible scheme, labeled as Initial, as $T$ increases, MSEE also gets increased. however, such monotonically increasing trend is not observed on the other schemes. Indeed, when the mission time increases, the MSEE performance improves due to more time for secure communications and adjusting flight parameters. However, the higher the mission time, the larger the mechanical power consumption. Therefore, the overall trade-off between these two phenomena, i.e., MASR and AFPC, results in the fact that the MSEE performance does not get monotonically increased, though following an overall increasing trend, as $T$ rises, e.g., from 8 to 9 s of MSEE-MI and MSEE-Seq curves, in contrast to the MASR metric studied in [13]. This illustrates the significance of considering propulsion power consumption for designing secure energy-efficient UAV-enabled systems. We also note that for a particular MSEE requirement, minimizing the task completion time of the considered UUR-system appears an interesting problem and requires deep investigation.

Fig. 9 illustrates the performance of MSEE with the increase of average network transmission power (ANTP) parameter, defined as $p^{\text{ave}}$ such that $p_{k}^{\text{ave}} = 0.1p^{\text{ave}}$, $p_{u}^{\text{ave}} = 0.5p^{\text{ave}}$, $p_{u}^{\text{ave}} = 0.4p^{\text{ave}}$. The curve labeled as Initial belongs to the MSEE performance of non-optimal feasible initialization. We again observe that the performance gaps that our joint designs offer are significantly higher than the other benchmark designs, and the relative gap, interestingly, slightly increases as the ANTP gets larger. For example, the MSEE-MI scheme improves the MSEE performance by approximately 16 Mbits/Joule when $p^{\text{ave}} = 1$ W; however, around 19 Mbits/Joule enhancement is achieved with $p^{\text{ave}} = 8$ W, in comparison with the Initial scheme.

In Fig. 10, the average flight power consumption ratio (AFPCR), defined as $\rho = \frac{P_{u}}{P_{\text{avg}}}$, is plotted against the flight power limit. It can be seen that the MSEE designs are more conservative than the MASR-Seq scheme when it comes to the AFPCR performance, particularly, both MSEE-MI and MSEE-Seq achieve the least ANTPR, comparatively. Further, we can construe that as the flight power limit decreases, the larger proportion of the dedicated UAV’s on-board battery resource is consumed throughout the mission.

V Conclusions

In this paper, we investigated the challenging task of designing an energy-efficient THz-UUR system for secure and periodically data delivering from multiple ground UEs towards the BS. For the fairness of QoS amongst the UEs, a MSEE maximization problem was formulated, by which the fundamental system parameters are designed to improve the overall system secrecy and energy-efficiency performance. This was formally posed as a challenging mixed-integer non-convex nonlinear maximin optimization problem. We then embarked on tackling the non-convexity of the formulated problem and
proposed low-complex BCD-SCA-Dinkelbach based iterative algorithms to solve it suboptimally with guaranteed convergence. Simulation results confirmed the fast convergence of our proposed algorithms, demonstrated significant MSEE performance improvement than the other benchmarks, and provided insightful results in the optimized system parameters such as UUR’s trajectory and velocity pattern as well as communication resource allocations, including transmit power profiles and user scheduling. Also, the effects of mission time, and molecular absorption factors arising from the THz links on the system MSEE performance have been examined. As future work, we will deeply investigate the dynamic topology of aerial platforms with more practical THz channel modeling while leveraging benefits of extreme directional beamforming for intelligent UUR systems as well as taking into account the mobility of terrestrial UE.

Fig. 6: Transmit power allocation and user scheduling against time for different schemes.

Fig. 7: Effect of THz molecular absorption on the MSEE.

Fig. 8: Effect of mission time on the MSEE performance.

**Appendix A**

**Proof of Lemma 1**

Computing the Hessian matrices of given functions yields

\[
\begin{align*}
H_1 &= \nabla^2 (Z_1) = \frac{c^2}{(x+cy)^2} \begin{bmatrix}
-\frac{y^2}{x} & y \\
-\frac{y}{x} & -x
\end{bmatrix}, \\
H_2 &= \nabla^2 (Z_2) = \begin{bmatrix}
-\frac{abx \sigma_3}{\sigma_2} \\
\sigma_1 \\
-\frac{abx^2 \sigma_3}{\sigma_2}
\end{bmatrix},
\end{align*}
\]

wherein \(\nabla^2(\cdot)\) denotes the hessian operator, and \(\sigma_1 \triangleq \frac{abx \sigma_3}{\sigma_2}, \quad \sigma_2 \triangleq (y+bx)^2((a+1)y+(a+2)bx), \quad \text{and} \quad \sigma_3 \triangleq 2(1+a)y+(a+2)bx.\)

One can verify that both matrices \(H_1\) and \(H_2\) are negative semidefinite \((H_{1,2} \prec 0)\), thereby functions \(Z_1\) and \(Z_2\) are jointly concave w.r.t \(x\) and \(y\). Accordingly, there exist global over-estimators for concave functions in (23), following
Fig. 9: Effect of average network transmission power on the MSEE performance.

Fig. 10: Effect of flight power limit on the average flight power consumption ratio.

We can verify that the first-order and second-order determinants of \( \mathbf{H}_{11} \) and \( \mathbf{H}_{12} \) are all non-negative, and therefore, the Hessian matrices are positive semi-definite (\( \mathbf{H}_{11(2)} \geq 0 \)), indicating that functions \( f_{41}(x, y) \) and \( f_{42}(x, y) \) are jointly convex w.r.t \( x \) and \( y \). Further, the convexity of \( f_{43}(x, r) \) and \( f_{44}(x, p) \) follows from (B.6) and [17, Lemma 1]. Given these functions are all convex, one can use the first-order Taylor expansions at points \( x_0 \) and \( y_0 \) to reach the global tight lower-bounds and inequalities in Lemma 2. The proof is completed.

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