Voids in the SDSS DR9: observations, simulations, and the impact of the survey mask

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ABSTRACT

We present and study cosmic voids identified using the watershed void finder VIDE in the Sloan Digital Sky Survey Data Release 9, compare these voids to ones identified in mock catalogs, and assess the impact of the survey mask on void statistics such as number functions, ellipticity distributions, and radial density profiles. The nearly 1,000 identified voids span three nearly volume-limited samples from redshift $z = 0.43$ to 0.7. For comparison we use 98 of the publicly available 2LPT-based mock galaxy catalogs of Manera et al., and also generate our own mock catalogs by applying a Halo Occupation Distribution model to an $N$-body simulation. We find that the mask reduces the number density of voids at all scales by a factor of three and slightly skews the relative size distributions. This engenders an increase in the mean ellipticity by roughly 30%. However, we find that radial density profiles are largely robust to the effects of the mask. We see excellent agreement between the data and both mock catalogs, and find no tension between the observed void properties and the properties derived from ΛCDM simulations. We have added the void catalogs from both data and mock galaxy populations discussed in this work to the Public Cosmic Void Catalog at http://www.cosmicvoids.net.

Key words: cosmology: observations, cosmology: large-scale structure of universe, methods: data analysis

1 INTRODUCTION

With the recent advent of large-scale comprehensive void catalogs (Pan et al. 2012; Sutter et al. 2012b), cosmological analysis is beginning to fan out from probes solely focused on overdensities such as galaxy correlations (Sanchez et al. 2012; Marin et al. 2013) and baryon acoustic oscillations (Bassett & Hlozek 2010) to more general studies based on alternative information sources available in the cosmic web. Since the primary target of cosmological analysis is often quantifying and understanding dark energy (Weinberg et al. 2013), exploiting the underdense voids in the matter distribution of the universe is a natural choice: the interiors of voids are dominated by dark energy (Goldberg & Vogeley 2004), so their shapes, sizes, and growth histories are intimately tied to the global properties of the large-scale universe (Thompson & Gregory 2011).

Already researchers have begun to exploit the public void catalogs. Ilie et al. (2013) correlated void positions with WMAP measurements of Cosmic Microwave Background temperature anisotropies (Komatsu et al. 2011) to obtain a weak measurement of the integrated Sachs-Wolfe effect (Thompson & Vishniac 1987). The Planck Collaboration followed up on this study to confirm a detection (Planck Collaboration 2013a). Melchior et al. (2014) have performed a measurement of gravitational weak lensing around voids...
in data (theoretically predicted by [Krause et al. 2013] and [Higuchi et al. 2013] to directly measure the underdensities in the dark matter. [Pisani et al. 2013] used a novel method to measure the real-space radial density profiles within voids without assumptions about cosmological or redshift-space distortion models. Finally, [Sutter et al. 2012a] began to measure cosmological parameters by leveraging the statistical isotropy of stacked voids ([Lavaux & Wandelt 2011]) to perform an Alcock-Paczynski test ([Alcock & Paczynski 1979; Ryden 1995]).

Looking ahead, there are many more promising applications of voids to cosmology and astrophysics. At the most simple level, the size distribution of voids is sensitive to cosmological parameters ([Jennings et al. 2013]) and modified gravity ([Champtit et al. 2013]), though these effects can be confused by uncertainties in galaxy formation physics ([Little & Weinberg 1994; Muller et al. 2000; Tinker & Conroy 2009]). A measurement of the shapes of voids as encoded by the mean ellipticity would shed light on dark energy ([Biswas et al. 2010; Bos et al. 2012]) as well as the two-point correlation of the void positions ([Padilla et al. 2005; Panajape et al. 2012; Hamaus et al. 2014]). The radial density profile, reconstructed in real space using techniques such as those described in [Pisani et al. 2013], can also be used to constrain exotic dark energy models ([Shoji & Lee 2012; Spolyar et al. 2013]). Astrophysically, voids can also be used to measure primordial magnetic fields ([Taylor et al. 2011; Beck et al. 2013]) and the effects of environment on galaxy formation ([Gottlober et al. 2003; Rojas et al. 2004; Hoyle et al. 2005; Rojas et al. 2006; Ferreras & Pasquali 2011; Ceccarelli et al. 2012; Hoyle et al. 2012]).

To support current and future void-based science efforts we must continue to identify voids in the latest galaxy surveys. This way we can take advantage of deeper and wider surveys for a greater redshift lever arm for cosmological parameter estimation and for more volume for increasing the signal-to-noise of statistical void properties. Also, even though current surveys such as the Baryon Oscillation Spectroscopic Survey (BOSS; [Dawson et al. 2013]) may not be optimal for void analysis due to their relatively low sampling density, we can use void catalogs from data to test and calibrate results against theoretical expectations in preparation for larger-volume surveys in the future such as Euclid ([Laureijs et al. 2011]), BigBOSS ([Schlegel et al. 2011]), and WFIRST ([Spergel et al. 2013]).

Ever since [Peebles 2001] pointed out a potential discrepancy between the interior contents of voids in ΛCDM predictions and observations, there has been intense interest in comparing voids between simulations and observations. This has been done for earlier void catalogs in the 2-Degree Field Galaxy Redshift Survey (2dFGRS; [Benson et al. 2003; Hoyle & Vogeley 2004; Ceccarelli et al. 2006]) and the Sloan Digital Sky Survey (SDSS; [Strauss et al. 2002]), Data Release 7 ([Pan et al. 2012]), and in earlier surveys ([Einasto et al. 1991; Weinberg & Cole 1992; Little & Weinberg 1994; Vogeley et al. 1994]) but in a very restricted context: it is difficult to build simulations with high enough resolution to capture all the survey galaxies and sufficient size to enclose the entire survey volume. Rather than attempt to reproduce complex observational details such as survey geometry, typically authors take a limited volume within the survey and compare the statistical properties of the remaining voids to voids identified in a galaxy population generated with semi-analytic modeling (e.g., [Tavassoli et al. 2013]). This common approach has several shortcomings: it is difficult to precisely tune semi-analytic models to a given survey ([Baugh et al. 2003]) and it does not take advantage of the full survey volume. We can address any potential discrepancies in a more robust way by building nearly identical survey-like populations in our simulations.

An examination of the impacts of the survey mask is especially important, since only selecting voids far away from the survey area discards much useful information, and without rigorous void selection there may still be residual systematics. Also, since theoretical work with voids is done in simulations with cubic volumes, understanding the role of the mask is essential for building the links between theory and data. Since survey masks usually have complicated shapes, their impact is highly non-trivial, non-obvious, and different for each survey. [von Benda-Beckmann & Mueller 2007] noted differences between masked and unmasked void populations in the 2dFGRS, although [Pan et al. 2012] did not find significant differences when examining the properties of voids with their void finding algorithm in a low-redshift volume-limited sample of SDSS galaxies. However, there has been no such examination in higher redshifts of the SDSS with the VIDE algorithm ([Sutter et al. 2014]), which is the source of the current large void catalogs.

We explore another important link, the impacts of sparsity and galaxy bias, in another work ([Sutter et al. 2014]), while earlier works such as [Ryden & Melott 1996] have connected redshift-space voids to those in real space.

In this work, we present voids in the SDSS Data Release 9 CMASS sample ([Ahin et al. 2012]), a survey covering 3,000 square degrees from redshift 0.43 to 0.7, for a total volume of nearly 1.5 cubic h⁻¹Gpc. We compare these voids to voids found in two sets of mock catalogs: the published mocks of [Manera et al. 2013] and our own derived from a large-volume high-resolution N-body simulation. In the simulation we are able to capture the entire survey without overlapping or stitching simulation volumes, allowing us to examine the systematic impacts of the survey mask on void statistical properties such as number functions, radial profiles, and ellipticities. While the low galaxy density of this survey is not ideal for void identification, the analysis of [Sutter et al. 2014] indicates that voids found in surveys of this type still correspond to physical underdensities in the dark matter, and thus are still useful probes of cosmology and astrophysics. In addition, [Sutter et al. 2014] shows that the universal density profile of [Hamaus et al. 2014] fits voids identified in all densities of samples, and that there exist simple scaling relations between voids in different samples, which means that the objects identified even in low-density surveys correspond to voids.

In the next Section we establish our coordinate system and briefly discuss our void-finding method and strategies for handling masks in the survey data. Section 3 introduces our galaxy survey samples and the properties of the voids identified in them. In Section 4 we present our mock galaxy populations and compare voids in these masked and unmasked populations to the voids in the data. Finally, Section 5 offers concluding remarks regarding implications for future surveys and void-based science.
2 VOID FINDING

For each galaxy in the survey, we transform its sky latitude $\theta$, sky longitude $\phi$, and redshift $z$, to a comoving coordinate system:

\[
x' = D_c(z) \cos \phi \cos \theta, \\
y' = D_c(z) \sin \phi \cos \theta, \\
z' = D_c(z) \sin \theta,
\]

where $D_c(z)$ is the comoving distance to the galaxy at redshift $z$. We assume a $\Lambda$CDM cosmology consistent with WMAP 7-year results [Komatsu et al. 2011]: $\Omega_M = 0.27$, $\Omega_\Lambda = 0.73$, and $h = 0.71$.

We identify voids with a modified and extended version of ZOBOT [Neyrinck 2008] [Lavaux & Wandelt 2011] [Sutter et al. 2012b]. called VIDE [Sutter et al. 2014]. VIDE creates a Voronoi tessellation of the tracer particle population and uses the watershed transform to group Voronoi cells into zones and voids [Platen et al. 2007]. The watershed transform identifies catchment basins as the cores of voids and ridgelines, which separate the flow of water, as the boundaries of voids. The watershed transform builds a nested hierarchy of voids [Lavaux & Wandelt 2011] [Bos et al. 2012], and for the purposes of this work we only examine root voids, which are voids at the base of the tree hierarchy and hence have no parents. We also impose two density-based criteria on our void catalog. The first is a threshold cut within VIDE itself where voids only include as additional members Voronoi zones with density less than 0.2 the mean particle density. If a void consists of only a single zone (as they often do in sparse populations) then this restriction does not apply. We apply the second density criterion as a post-processing step: we only include voids with mean central densities below 0.2 the mean particle density. We measure this central density within a sphere with radius $R = 0.25 R_{\text{eff}}$, where

\[
R_{\text{eff}} \equiv \left( \frac{3}{4 \pi V} \right)^{1/3}.
\]

In the expression above, $V$ is the sum of the Voronoi volumes of the particles which comprise the void. We also ignore voids with $R_{\text{eff}}$ below the mean particle spacing of the tracer population.

Additionally, for the analysis below we need to define a center for the void. For our work, we take the macrocenter, or volume-weighted center of all the Voronoi cells in the void:

\[
X_v = \frac{1}{\sum_i V_i} \sum_i x_i V_i,
\]

where $x_i$ and $V_i$ are the positions and Voronoi volumes of each tracer $i$, respectively.

As presented in [Sutter et al. 2012b] and [Sutter et al. 2014], VIDE includes modifications to ZOBOT to account for survey boundaries, internal masks, and redshift limits. To handle line-of-sight boundaries and internal masks, we pixelize the survey region using HEALPix [Gorski et al. 2005] and identify boundary pixels (i.e., pixels with at least one non-survey region neighbor). We inject particles along the line of sight within each boundary pixel with a spatial density of $10^{-3} (h^{-1} \text{Mpc})^{-3}$. By giving these boundary particles essentially infinite density and breaking their degeneracies in the Voronoi graph, we prevent the watershed algorithm from growing voids outside the survey region. Also, these boundary particles serve as a marker for identifying voids near the edge. Figure 1 shows our identification of the SDSS DR9 [Ahn et al. 2012] survey boundary pixels. To accurately capture the shape of the mask we required a resolution of $N_{\text{side}} = 512$ (~ $2 - 3 h^{-1} \text{Mpc}$ at $z = 0.7$ in a $\Lambda$CDM universe).

Following the procedure described in [Sutter et al. 2012b], we generate two void catalogs for each sample, which we call all and central catalogs. Naturally, the all sample contains every identified void which satisfied the density cutoff criteria, even voids near the survey edge. On the other hand, central voids do not touch any boundary particle (i.e., the most distant void member particle is closer than any boundary particle), and thus are not near any survey boundary or internal mask. The central sample is designed to ensure that we have a fair distribution of void shapes and alignments within the survey volume. To handle survey high-redshift caps, we simply exclude from all catalogs any void which extends beyond the redshift limits of a given sample. This is a more restrictive approach than the procedure discussed in [Sutter et al. 2012b], since it is difficult to construct stable tessellations on co-spherical points. To evaluate this, if the distance from the void macrocenter to the redshift edge is closer than the distance to any void member particle, we reject the void.

3 VOIDS IN DATA

3.1 Galaxy Populations

We take our galaxy sample from the CMASS selection of SDSS DR9 (BOSS) spectroscopic targets [Ahn et al. 2012]. This is the same sample of galaxies used in the analysis of [Reid et al. 2012]. The 455,281 galaxies in this selection of the survey extend from $z = 0.43$ to $z = 0.7$. As before in our catalog of voids in SDSS DR7 [Sutter et al. 2012b], we take volume-limited samples to ensure statistical uniformity and constant shot noise and galaxy bias around our identified voids. Also, we require volume-limited samples in order to compare to our mocks based on Halo Occupation

Figure 1. HEALPix map in a Mollweide projection of identified boundary zones (black) around and within the SDSS DR9 survey area where we inject boundary particles.
Distribution (HOD) models, which are constructed around volume-limited surveys (Berlind & Weinberg 2002).

We apply simple evolution and K-corrections of the form

\[ z_e = -2(1 - z + 0.1)(z - 0.1) \]
\[ z_k = -0.242659 + 1.38731z, \]

and compute absolute magnitudes \( M_e \) assuming the cosmological parameters noted above. We choose three redshift bins. Each redshift range is characterized by a typical galaxy luminosity, which we differentiate by the labels \( dim, mid, \) and \( bright \). Our redshift bins are: 0.43 < \( z < 0.5 \), which we label \( CMASS \; Dim \), 0.5 < \( z < 0.6 \), labeled as \( CMASS \; Mid \), and 0.6 < \( z < 0.7 \), called \( CMASS \; Bright \). Table 1 lists the sample name, limiting absolute magnitude, redshift bound, comoving volume, number of galaxies, and the mean galaxy separation in that sample. The mean galaxy spacing is \( (n_g/V)^{-1/3} \), where \( n_g \) is the number of galaxies within each sample and \( V \) is the sample volume.

Figure 2 shows the galaxy number density as a function of redshift for each of our samples. These plots show that a simple luminosity cut does not produce a truly volume-limited sample due to the complex target selection procedure in CMASS. The density in the \( Dim \) sample varies by a factor of \( \sim 4 \), in the \( Mid \) sample by a factor of \( \sim 2 \), and in the \( Bright \) sample by a factor of \( \sim 3 \). While we can account for redshift dependence in the densities by weighting individual galaxies in the VIDE code (Neyrinck 2008), our testing has shown that this does not strongly impact void properties, for two reasons. First, only the largest voids will span a deep enough redshift range to be sensitive to changes in the underlying density, and since the number of large voids are exponentially suppressed (and they are more likely to be removed from consideration because they intersect an internal boundary), varying galaxy number density will only affect a small percentage of voids. Secondly, the nature of the watershed algorithm naturally guards against effects of varying density: since each particle has on average 17 adjacent particles (Neyrinck 2008), we must reduce the local density of a wall by a large factor before it is no longer identified as a void boundary.

Table 2. Summary of voids in data.

| Sample Name       | \( z_{min} \) | \( z_{max} \) | Volume \((h^{-3} \text{Gpc}^3)\) | \( N_{voids} \) |
|-------------------|--------------|--------------|---------------------------|----------------|
| \( CMASS \; Dim, \; all \) | 0.43 | 0.5 | 0.29 | 283 |
| \( CMASS \; Dim, \; central \) | 0.43 | 0.5 | 0.29 | 151 |
| \( CMASS \; Mid, \; all \) | 0.5 | 0.6 | 0.53 | 570 |
| \( CMASS \; Mid, \; central \) | 0.5 | 0.6 | 0.53 | 242 |
| \( CMASS \; Bright, \; all \) | 0.6 | 0.7 | 0.66 | 283 |
| \( CMASS \; Bright, \; central \) | 0.6 | 0.7 | 0.66 | 137 |

Table 2 summarizes the data samples used in this work, the redshift ranges used to produce the void samples, their respective volumes, and the total number of voids identified in each sample. In total, we identify nearly 1,000 voids in the \( all \) sample, while the \( central \) sample produced \( \sim 480 \) voids.

### 3.2 Void Properties

Figure 3 shows the distribution of void sizes as a function of redshift for all the galaxy samples. We show both \( all \) and \( central \) voids. We see that though a few voids in \( CMASS \; Mid \) and \( CMASS \; Bright \) reach an effective radius of \( \sim 80 \; h^{-1}\text{Mpc} \), most — especially in the \( central \) catalog — are below 50 \( h^{-1}\text{Mpc} \). For \( Mid \) and \( Bright \) samples, voids pervade the low-redshift boundary, because here we keep the population of galaxies below that boundary and only reject voids whose centers fall below the redshift cutoff. On the other hand, we see a tapering in the distribution at the high-redshift caps: here, we reject any void that might intersect the cap, and we are more likely to cut progressively larger voids. We remove even more of the largest voids when creating the \( central \) samples, since these voids are more likely to lie nearby the mask line-of-sight boundaries. We observe a distinct lack of small voids in the \( Bright \) sample, which is a consequence of its slightly lower mean galaxy spacing. While we expect to see smaller voids at higher redshift, the effects of sparsity and biasing lead to larger observed voids (D’Aloisio & Furlanetto 2007).

We show another way of expressing the size distribution in Figure 4. This is a plot of the cumulative number function: the total number of voids in each sample above a given effective radius. The number function is a potentially powerful probe of cosmology with voids (Sheth & van de Weygaert 2004). All samples have roughly the same number density of the largest voids, but the lack of smaller voids in the \( CMASS \; Bright \) sample manifests as a uniformly reduced number function for small- and medium-scale voids. In all samples, the \( central \) catalogs host roughly half as many voids as the \( all \) catalogs. This is a consequence of the relatively large surface-to-volume ratio of the current CMASS survey. The relatively narrow angular extent especially impacts our void populations; the small internal holes do little disruption. As future data releases fill in the central regions of the expected coverage area, we should approach the higher fraction of \( central \) voids seen in earlier surveys (Sutter et al. 2012b).

Though voids have complex shapes, we can assign them a unique ellipticity. This simple scalar captures most of the shape information of the void, and its distribution is a sen-
Table 1. Volume-limited galaxy samples used in this work.

| Sample Name   | $M_{r,\text{max}}$ | $z_{\text{min}}$ | $z_{\text{max}}$ | Volume ($h^{-3}\text{Gpc}^3$) | $N_{\text{gal}}$ | $n_{-1/3}$ ($h^{-1}\text{Mpc}$) |
|---------------|---------------------|-------------------|-------------------|-------------------------------|------------------|-------------------------------|
| CMASS Dim     | -20.1               | 0.43              | 0.5               | 0.29                          | 61249            | 16.76                         |
| CMASS Mid     | -20.1               | 0.43              | 0.6               | 0.82                          | 188300           | 16.29                         |
| CMASS Bright  | -20.8               | 0.43              | 0.7               | 1.48                          | 205732           | 19.29                         |

Figure 3. Distribution of voids within the CMASS samples. We plot void effective radius $R_{\text{eff}}$ (Eq. 1) versus redshift. We show the voids in the volume-limited samples CMASS Dim (red), CMASS Mid (blue), and CMASS Bright (green). All voids are marked with a cross, and voids in the central catalog are marked by filled circles.

Figure 4. Cumulative void number function for CMASS Dim (red), CMASS Mid (blue), and CMASS Bright (green). The number functions of all voids, including those near survey boundaries and internal masks, are shown as solid lines, while central catalog voids are shown as dotted lines.

Figure 5 shows the distribution of ellipticities for each of our samples. The ellipticities for all the samples are remarkably consistent, with means $\sim 0.2$ and a slight skew in the distribution favoring slightly more elliptical voids. The central catalog of the CMASS Bright voids contains a few highly elliptical voids. While similar voids exist in all samples, the limited number of total voids in this sample leads to a highly lopsided distribution. In the same figure, we also show the mean ellipticity and the standard error on the mean (i.e., $\sigma/\overline{n}$, where $\sigma$ is the standard deviation and $\overline{n}$ is the number of voids) for each sample. The means broadly agree, with the CMASS Mid sample favoring slightly more spherical voids. The ellipticities in the central catalogs are different than those in all catalogs. We will see below that the mean ellipticity is sensitive to the distribution of void sizes in a particular sample. Since the mask affects the void size distribution in a non-trivial way for each sample, depending on the relative surface-to-volume ratio in the sample, we should not be surprised to measure slightly different mean void ellipticities. Fortunately, this does not appear to be a large effect from sample to sample, and we conclude that we only need to understand mask effects for a particular survey geometry, not for individual volume-limited samples within that survey.

In Figure 6 we give a visual impression of some of the identified voids. We chose the particular slices randomly but selected a representative sample from the range of scales in the void catalog. We represent the selected void as collections of overlapping circles, where each circle is a void member galaxy with radius equal to the effective radius of each Voronoi cell. We overplot these circles on slices from the galaxy distribution. We see that voids at all scales indeed sit within underdensities in the galaxy distribution, though in some samples the sparsity makes it difficult to clearly distinguish the surrounding walls and filaments. However, our
analysis in Sutter et al. (2014) and Hamaus et al. (2014) show that these objects share common features with voids in high-density surveys.

Figure 7 shows one-dimensional radial density profiles of stacked voids in each sample. To compute the profiles, we take all voids in a sample of a given size range (e.g., 20 – 25 $h^{-1}$Mpc), align all their macrocenters, and measure the density in thin spherical shells. We normalize each density profile to the mean number density of the sample and show all profiles as a function of relative radius, $R/R_{eff}$. We only show profiles from the central voids of the samples. We show four stacks: 20-25, 30-35, 40-45, and 50-55 $h^{-1}$Mpc.

The smallest stack, 20-25 $h^{-1}$Mpc, is very close to the mean galaxy separation for the samples, and this manifests in an extremely steep profile. While these small voids may be unreliable due to Poisson shot noise, we do not assess statistical significance in this work. We believe that the common technique used with watershed algorithms (comparing to voids in a Poisson distribution of equal number density) is inadequate because small voids tend to appear in higher density regions, and thus are more likely to be real voids than one would expect. We are currently developing a more robust significance criteria based on Bayesian analysis of constrained realizations of a given sample.

As we progress to larger stacks, the profiles become more shallow and the overdense region surrounding the voids becomes less pronounced, as also seen in Ceccarelli et al. (2013). However, as before in the voids of SDSS DR7 (Sutter et al. 2012b), we see a qualitatively universal profile across all void sizes and redshift ranges: an underdense center, a steep power-law slope at the wall of the void, a slightly over-dense “compensation”, and a steady declining to the mean density. We see here that there is a larger difference among the samples than in the DR7 voids. A significant reason for this is the smaller survey area: while we guarantee central voids to sit completely within the survey, these profiles extend beyond the void effective radius. Since the survey area is relative small, the profile quickly reaches into volumes beyond the survey mask. There are also boundary particles at the edges. Depending on the relative density of the boundary particles and the location of stacked voids relative to the boundary we see different profiles at larger radii. Within $R_{eff}$, we see strong consistency among the samples, as expected. The number of voids in the stack strongly affects the smoothness of the profile. In particular, the 50-55 $h^{-1}$Mpc stack in CMASS Mid contains only 5 voids, which leads to a highly irregular profile shape.

4 VOIDS IN MOCKS

4.1 Mock Galaxy Populations

We take several avenues for comparison to the voids in the survey data. For the first set of mocks, we compute a single ΛCDM dark matter $N$-body simulation, extract halos from the simulation, and use the halos positions and masses as inputs for an HOD model. For the simulation we use the 2HOT code, an adaptive tree code N-body method whose operation count scales as $N \log N$ in the number of particles (Warren 2013). Accuracy and error behavior have been improved significantly for cosmological volumes through the use of a technique to subtract the uniform background density, as well as using a compensating smoothing kernel for small-scale force softening (Dehnen 2001). We use a standard symplectic integrator (Quinn et al. 1997) and an efficient implementation of periodic boundary conditions using a high-order ($p = 8$) multipole local expansion. We adjust the error tolerance parameter to limit absolute errors to 0.1% of the rms peculiar acceleration. As an example, a complete $4096^3$ particle simulation requires about 120 wall-clock hours using 12,000 CPU cores. Initial conditions were generated using a power spectrum calculated with CLASS (Blas et al. 2011) and realized with a modified version of 2LPTIC (Croccolo et al. 2006).

This particular simulation assumed Planck first-year cosmological parameters (Planck Collaboration 2013b). The box size was $4h^{-1}$Gpc on a side and contained $4096^3$ particles, giving a particle mass resolution of $7.36 \times 10^{10} h^{-1} M_\odot$. All analysis in this work used a single snapshot at $z = 0.53$. We identified halos in the simulation volume using the Rockstar halo finder (Behroozi et al. 2013), a six-dimensional phase-space plus time halo finder, to identify spherical overdensity (SO) halos at 200 times the background density. We use the default Rockstar parameters, except for requiring strict SO masses which includes un-
assigns central and satellite galaxies to a dark matter halo HOD model described in Zheng et al. (2007). HOD modeling using the code described in Tinker et al. (2006) and the bound particles and particles which may exist outside of the halo. We produce galaxy catalogs from the halo population using the code described in Tinker et al. (2006) and the same HOD prescriptions and allows us to gauge the range of void statistics predicted from simulations. We call these samples Masked N-body Mock. Taken together, we find ∼3,300 voids in the all samples of all orientations, and ∼1300 voids in the central samples.

For the full-volume simulation analysis, we use the entire three-dimensional volume of the simulation box and perturb each galaxy according to its peculiar velocity. We call this full-volume set of mock galaxies the N-body Mock sample. Even though we analyze only a single realization, the large volume produces over 90,000 voids.

To provide a more direct comparison to the data and to understand the effects of the mask on void properties, we apply the same survey geometry to mock galaxies as is used in the SDSS DR9 samples. Instead of placing galaxies in redshift space along the z-axis of the simulation box as we do above, we place an observer at the center of the volume and measure each galaxy position as its radial distance from that observer. We also perturb the galaxies according to the peculiar velocities in all directions. We project all galaxies onto the sky and apply the mask in Figure 1. Since we wish to compare solely to the CMASS Mid sample, we only take mock galaxies within 0.43 < z < 0.5. For void finding we treat this sample exactly as data: we deploy boundary particles and we build all and central catalogs of voids. While it is very expensive to compute multiple realizations with this volume and resolution, we can take advantage of the relative narrowness of the current DR9 survey by rotating our mask orientation within the same simulation volume. We take 5 separate orientations. Even though these samples are not quite independent, and we are likely to not capture enough of the very largest voids due to finite-volume effects, this technique still provides a good proxy for multiple realizations and allows us to gauge the range of void statistics predicted from simulations. We call these samples Masked N-body Mock. Taken together, we find ∼3,300 voids in the all samples of all orientations, and ∼1300 voids in the central samples.

Since high-resolution N-body simulations are very expensive, and the galaxy correlation analysis of Reid et al. (2012) required many mocks for estimating shot noise, the BOSS team produced many mock catalogs based on second-order Lagrangian perturbation theory (2LPT) with a WMAP 7-year cosmology and the same HOD prescription described above (Manera et al. 2013). We used 98 of...
Figure 7. One-dimensional radial density profiles of stacked voids. Each profile is normalized to the mean number density $\bar{n}$ of that sample and $R_{eff}$ corresponds to the median void size in the stack. We only show profiles from stacked central voids. Void profiles do not necessarily reach the mean density because of the influence of boundary particles and empty regions outside the survey volume. The caption lists the number of voids stacked in each profile.

Finally, to evaluate the significance of our ellipticity measurements, we identified voids in a single random realization provided by the CMASS team. In this realization, galaxies are randomly distributed with Poissonian statistics within the survey volume.

Table 3 summarizes the mock samples used in this work, their respective volumes, the number of independent mock samples, and the total number of voids identified in each sample.

### Table 3. Summary of voids in mocks.

| Sample Name                | Volume $(h^{-3}\text{Gpc}^3)$ | # Mocks | $N_{\text{voids}}$ |
|---------------------------|---------------------------------|---------|-------------------|
| N-body Mock               | 64.00                           | 1       | 91711             |
| Masked N-body Mock, all   | 0.53                            | 5       | 3336              |
| Masked N-body Mock, central | 0.53                        | 5       | 1313              |
| Masked 2LPT Mock, all     | 0.53                            | 98      | 56096             |
| Masked 2LPT Mock, central | 0.53                            | 98      | 25299             |

4.2 Comparison to Data

Our first point of comparison is the cumulative number function. In Figure 8 we compare the number function of voids in the CMASS Mid data sample to all our mocks. First, the unmasked N-body Mock simulation hosts roughly three times as many voids per unit volume than the data, even though they have similar galaxy populations. This occurs at all scales, though there are ~ 4 times as many small voids.
void sizes than the N-body show much less variance at small void sizes and reach larger numbers for both all catalogs, we see excellent agreement in the number function. The different orientations of the N-body mocks are limited by the cosmic variance of a single simulation, so it is not surprising that we are not able to match the void number function at the largest void sizes. However, with the 2LPT mocks, we are able to capture the very largest voids. [Tavalesi et al. (2013)] first pointed out a potential tension between ΛCDM model and data, but we see no indication of this tension in our results.

Figure 8 shows the ellipticity distributions and mean ellipticities, identically to Figure[5]. In this plot, we compare CMASS Mid ellipticities to those found in mock samples. Voids in all mock and data samples tend to be more elliptical than voids drawn from Poissonian distributions (which give ϵ ∼ 0.12) , confirming the analysis of Sutter et al. (2014), which showed that ellipticity is a robust measurement even in low-density samples such as SDSS DR9.

As we saw earlier for the cumulative number functions, we find agreement between data and theoretical expectations in the form of mock catalogs only when we apply the mask: then the distributions are nearly identical. The all void samples agree among all the masked mocks and data. The mean ellipticities of the central Masked N-body Mock are slightly more than 2σ discrepant than the data, while the Masked 2LPT Mocks have much better agreement with the data. The differences between the N-body and 2LPT mock populations are not surprising since they have slightly different cosmologies, and the ellipticity is a very sensitive probe of cosmological parameters [Biswas et al. 2010; Bos et al. 2012]. Also, the 2LPT Mocks cover multiple realizations, whereas the N-body mocks are restricted to a single simulation. With the exception of the Masked N-body Mock, we see the same relationship between all and central ellipticities as in the data: voids in central samples less spherical. Indeed, the 90,000 voids in all the 2LPT mocks reduce the uncertainties to such a degree that this difference is easily distinguishable.

Voids in the data and masked mocks are more elliptical than in the full-volume simulation. We can understand the impact of the mask by examining the relationship between ellipticity and void size, as we show for the masked and unmasked N-body mocks in Figure[10]. The cause of the shift in ellipticities when masking data is readily apparent: larger voids tend to be more spherical, and their exclusion from the masked catalogs increases the overall mean ellipticity. The uncertainties in the N-body mocks are too large to distinguish any differences.

We derive the theoretical ellipticity distribution from DIVA [Lavaux & Wandelt 2010] with the rescaling parameter α = 0.25, as discussed in the analysis of Sutter et al. (2014). DIVA requires a void size distribution as input, and we take the actual distribution from the CMASS Mid central sample (i.e., Figure[4]). This choice of rescaling parameter α provided good agreements with mock void populations, and again here we see agreement with data, indicating a relationship between the sizes of voids identified with the watershed transform and their dynamical cores.

Interestingly, we see almost no significant differences between masked and unmasked radial density profiles, as we show in Figure[11]. Here we compare the unmasked N-body Mock and the Masked 2LPT Mocks to the CMASS Mid data sample. We do not plot stacks from the Masked N-body Mock since they simply overlap the existing curves but have larger scatter. The stacks shown here are the same as before.
Figure 9. Comparing the ellipticity distributions (left) and mean ellipticities with their uncertainties (right) of the CMASS Mid sample to the various mocks. Error bars are the same as indicated for Figure 5. The violet-colored distribution is the theoretical expectation from DIVA (Lavaux & Wandelt 2010) with the rescaling parameter $\alpha$ set to 0.25. DIVA predicts the ellipticity distribution from the size distribution of voids in the CMASS Mid central sample.

Figure 10. Distribution of ellipticities $\epsilon$ in small bins of effective radius $R_{\text{eff}}$ in the masked (green) and unmasked (red) N-body Mock simulations. The solid line shows the mean, and the shaded region is the 1$\sigma$ interval.

in Figure 9. With very few exceptions, profiles from both the data and the full-volume mock sit within the range of profiles constructed in the different realizations of the masked mock. This agreement persists at all void scales. The two visible excursions from the mocks is consistent with statistical expectations. Since radial density profiles by definition probe the interiors and immediate surroundings of voids, they naturally are more robust against distortions due to the mask. Also, the process of stacking turns sets of elliptical voids with different orientations into a roughly spherical shape, regardless of the distribution of the individual ellipticities (Lavaux & Wandelt 2011; Pisani et al. 2013). Thus any changes to the mean ellipticity due to the mask will not change the radial profiles significantly.

With the enormous number of voids in the N-body Mock sample, we begin to see the transition from over- to under-compensated voids (Hamaus et al. 2014). However, this transition is not clear in the data due to the lack of voids at these extreme scales.

5 CONCLUSIONS

We have constructed a void catalog from the SDSS DR9 CMASS spectroscopic galaxy survey. Combined with the voids from DR7, this is the largest void catalog to date. We have used previously-established methods for removing voids near survey boundaries to produce a catalog of voids with a fair distribution of shapes. This catalog also provides the most distant voids ever detected, extending our knowledge of galaxy underdensities to redshift $z = 0.7$. Our voids have effective radii between 20 and 70 $h^{-1}$Mpc, and exhibit the same qualitatively universal radial density profile seen in earlier works (Sutter et al. 2012b; Ceccarelli et al. 2013).

We used Halo Occupation Distribution modeling to produce mock catalogs for comparison purposes.

We find that the effects of the mask are highly non-trivial and can depend strongly on the relative surface area of the mask compared to the volume, the depth of the survey, the number of internal holes, and the detailed shape of the boundary. Cosmological statistics based on global void properties, such as number functions and ellipticity distributions, are especially vulnerable to the properties of the mask. However, we find that probes based on void interiors, such as radial density or velocity profiles, are generally more robust. Also, cosmological applications which depend on the statistical isotropy of voids, such as the Alcock-Paczynski test (Sutter et al. 2012a), are resilient. In cases such as this, while the mask may change the average void shape or size, as long as the mask preserves a uniform sampling of their orientations then the methods are sound.

Furlanetto & Piran (2006) and Tinker & Conroy (2009) hypothesized that the so-called “void phenomenon” of Peebles (2001) can be explained by galaxy bias. This has led to a general discussion in the literature about potential discrepancies between the voids in theory and voids in data. For the void definition we adopt, abundances, ellipticity distributions, and radial profiles all indicate that voids in simulations have the same sizes, shapes, and interior contents as observed voids once galaxy bias, sparsity, and survey masks are accounted for. Overall, we find no significant discrepancies between observations of voids in the SDSS DR9 and $\Lambda$CDM mocks.

We have made all the SDSS DR9 voids, as well...
Figure 11. Comparison of one-dimensional radial density profiles. The void stacks and normalizations are the same as in Figure 7. The solid red lines are profiles from CMASS Mid, the solid green lines are from the full-volume unmasked N-body Mock, while the shaded blue region shows the full range of profiles from the 98 realizations of the Masked 2LPT Mock simulations. The caption lists the number of voids stacked in each profile, except for Masked 2LPT Mock, where the caption shows the mean number of voids in each realization for that stack. The number of excursions of the data from the mocks is consistent with expectations.

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