Single-shot measurement of longitudinal phase space beam profile in an electron storage ring

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A novel scheme to measure the longitudinal emittance and phase space profile in an electron storage ring by using correlations between time and the vertical coordinate, and between energy and the horizontal coordinate, is proposed. This longitudinal profile measurement scheme will help to demonstrate recent results of advanced studies for manipulating the longitudinal beam profile and for investigating beam instability in an electron storage ring.

1. Introduction

Transverse bunch crabbing using a two-frequency crab cavity scheme (Zholents, 2015; Huang et al., 2019) provides the optimal solution to produce short-pulse (1–10 ps full width at half-maximum) X-rays in a storage ring. This scheme would enable increased precision of timing-mode studies of a large number of dynamic processes in materials as they function. A crab cavity can also be used as an injection kicker in a new on-axis injection scheme (Kim et al., 2019) that uses a transverse deflecting radio-frequency (RF) cavity to kick the incoming beam into an already populated bucket but with a timing offset from the synchronous phase.

A crab cavity can also be used to measure bunch length (Loew & Altenmueller, 1965; Emma et al., 2000). A crab cavity couples the y–z or x–z planes, so bunch length is projected in the y or x dimension, respectively. The resolution of this bunch length measurement is limited by transverse emittances \( \varepsilon_x \) and \( \varepsilon_y \) unless a specialized beam transport line such as a chicane (Xiang & Ding, 2010) is used. Regardless of using a crab cavity, the distribution of the energy deviation \( \delta = \frac{dp}{p} \) of a bunch can be projected in the x dimension at which horizontal dispersion \( \eta_x \) is large. The resolution of this is limited by the ratio \( \varepsilon_x/\eta_x \). Combining these two principles enables measurement of the longitudinal profiles (z–\( \delta \)) of a bunch in the x–y plane.

A fourth-generation storage ring (4GSR) is an accelerator that provides small emittance so that the measurement can be made with high resolution. A 4GSR adopts a multi-bend achromat (MBA), that effectively suppresses natural emittance. The MAX IV 4GSR is currently operating; others, including APS-U, SPring-8-II, SLS-II, ALS-U, SIRIUS, ESRF-EBS and Korea-4GSR, are being designed, constructed or commissioned [Streun, 2017; Steier et al., 2016; Liu et al., 2013; see also design reports for MAX IV (https://www.maxiv.lu.se/acceleratorsbeamlines/accelerators/acceleratordocumentation/max-iv-ddr), APS Upgrade (https://www.aps.anl.gov/APSUpgrade), SPring-8-II (http://rsc.riken.jp/...
Definitions of each matrix element can be found in Appendix A. When initial beam coordinates at the position 1 are given as \( X_1 = (x_1, x'_1, y_1, y'_1, z_1, \delta_1) \), its continuous mapping via \( T_c \) and \( M_{12} \) becomes

\[
X_2 = M_{12} T_c X_1 = \begin{pmatrix}
R_{11} x_1 + R_{12} x'_1 \\
+ (\eta_2 - R_{11} \eta_1 - R_{12} \eta'_1) y_1 \epsilon \\
+ (\eta_2 - R_{11} \eta_1 - R_{12} \eta'_1) \delta_1 \\
R_{21} x_1 + R_{22} x'_1 \\
+ (\eta'_{21} - R_{21} \eta_1 - R_{22} \eta'_1) y_1 \epsilon \\
+ (\eta'_{21} - R_{21} \eta_1 - R_{22} \eta'_1) \delta_1 \\
R_{33} y_1 + R_{34} y'_1 + R_{34} z_1 \epsilon \\
R_{43} y_1 + R_{44} y'_1 + R_{44} z_1 \epsilon \\
A x_1 + B x'_1 + (C - A \eta_1 - B \eta'_1) y_1 \epsilon + (C - A \eta_1 - B \eta'_1) \delta_1 \\
y_1 \epsilon + \delta_1
\end{pmatrix}.
\]  

Let us assume that position 1 is located at one of the achromats of a storage ring (\( \eta_1 = 0 \)), and position 2 is at a point that has large dispersion. If \( \psi_x \simeq (2n + 1) \pi \) and \( \psi_y \simeq [(2n + 1)/2] \pi \), contributions from \( R_{34} \) and \( R_{44} \) are negligible. The magnitude of \( R_{11} \) is approximately \((\beta_{12}/\beta_{11})^{1/2}\) when \( \psi_x \simeq (2n + 1) \pi \), and it is conservatively less than 3 as the ratio of \( \beta_{12} \) over \( \beta_{11} \) is less than 10 for most lattices. Specifically, when emittance \( \simeq 100 \) pm, \( \delta_1 \simeq 0.001 \) and \( \eta_2 \simeq 0.10 \) m, the contribution from \( \eta_2 \sigma_{\eta_1} \) at \( x_2 \) is one order larger than that from \( \sigma_{\psi_1} \) \((i.e. \sigma_{\psi_1} \simeq 10^{-5} \) m and \( \eta_2 \sigma_{\eta_1} \simeq 10^{-4} \)), which means we can expect projection between \( x_2 \) and \( \eta_2 \sigma_{\eta_1} \). Likewise, \( y_2 \) is dominated by \( R_{34} z_1 \epsilon \) as \( \sigma_{\psi_1} \) of the order of \( 10^{-6} \) but \( z_1 \) is of the order of \( 10^{-3} \) and \( \epsilon \) has order \( 10^{-2} \). Clearly, smaller emittance will lead to better resolution.

Hence, \( x \) and \( y \) coordinates at position 2 are expressed as

\[
\begin{pmatrix}
x_2 \\
y_2
\end{pmatrix} \approx \begin{pmatrix}
0 \\
R_{34} \epsilon
\end{pmatrix} \begin{pmatrix}
\eta_2 \\
0
\end{pmatrix} \begin{pmatrix}
\epsilon \\
\delta_1
\end{pmatrix}.
\]

which shows the projection of the \( z-\delta \) plane onto the \( x-\gamma \) plane. Its resolution is mainly dependent on whether the contributions from \( x_1, x'_1, y_1 \) and \( y'_1 \) are negligible and whether \( \psi_x \simeq (2n + 1) \pi \) and \( \psi_y \simeq [(2n + 1)/2] \pi \). If they are, then \( R_{34} \) has \( \sin(\psi_x) \) dependence, so large \( \eta_2 \) leads to increased magnification for the \( x \) plane, and \( \psi_y \) close to \([(2n + 1)/2] \pi \) leads to increased magnification for the \( y \) plane.

A hybrid MBA lattice such as ESRF-EBS, APS-U, PAL-4GSR satisfies the above-described conditions. Due to the common \((\psi_x, \psi_y) = (3\pi, \pi)\) phase advance between two dispersion bumps in a cell of a hybrid MBA lattice, each cell has a similar phase advance. Specifically, a hybrid MBA lattice has \( \psi_x \simeq 0.9 \pi \) and \( \psi_y \simeq 0.4 \pi \) from the center of the long straight section to the nearest dispersion bump. Hence, choosing the position of a crab cavity satisfying \( \psi_y = 0.5 \pi \) is accompanied by \( \psi_x \simeq \pi \).

3. PAL-4GSR and the intrinsic resolution

The PAL-4GSR storage ring is a hybrid seven-bend achromat (H7BA) lattice with a horizontal emittance of 90 pm. The
The PAL-4GSR lattice (Table 1, Fig. 1) contains a 2 T super-bend in the central dipole to produce radiation with a critical energy of 12 keV. The concepts of the ESRF-EBS and APS-U lattices were adopted in the PAL-4GSR lattice. The dispersion was deliberately enlarged between the first and second dipoles and between the sixth and seventh dipoles, then three chromatic sextupoles were located in this dispersion bump region to reduce the strength required to control the chromaticity. The betatron phase advances between the two dispersion bumps were set to $\Delta \varphi_x \simeq 3\pi$ in the horizontal plane and $\Delta \varphi_y \simeq \pi$ in the vertical plane; as a result, nonchromatic effects of the sextupoles are canceled out naturally. To minimize natural emittance, five-step longitudinal gradient dipoles and reverse bending magnets were considered (Streun & Wrulich, 2015; Nagaoka & Wrulich, 2007; Delahaye & Potier, 1989; Streun, 2014).

We performed tracking simulation to examine the resolution of the measurement using a transverse deflecting cavity (TDC) on PAL-4GSR. For tracking simulation, we used elegant software (Borland, 2000). A total of 100000 particles were generated at the position of the TDC (Fig. 1). They have a 58 pm (standard deviation) Gaussian distribution with matched Twiss functions in the horizontal and vertical planes, and ten lines of uniform density with maximum values of $1/\Delta \varphi_x = 0.3\%$ and $1/\Delta \varphi_y = 24$ mm in the longitudinal plane (Fig. 2). A watching point located at the left dispersion bump has a vertical phase advance of $\Delta \varphi_y = 2$ from the position of the TDC. For a TDC, we set a voltage of 4.5 MV and a frequency of 750 MHz, which yield $1/\Delta \varphi_x = 0.02358$. When the TDC was off, we observed five resolved distributions on the $x$ axis at the watching point due to the correlation $x_2 \simeq \eta_2 \delta_z$ [Figs. 3(a) and 4(a)]. In the $y$ axis, the distribution was not resolved [Figs. 3(a) and 4(b)]. Standard deviations of Gaussian peaks were

Table 1
Parameters relevant to the PAL-4GSR lattice.

| Parameter                          | Value     | Unit  |
|-----------------------------------|-----------|-------|
| Energy                            | 3         | GeV   |
| Emittance (flat / round)          | 90 / 58   | pm    |
| Circumference                     | 569.96    | m     |
| Tune ($x / y$)                    | 47.545 / 18.203 |       |
| Natural chromaticity ($x / y$)    | $-96.0 / -57.9$ |       |
| Radiation loss per turn           | 0.468 (without insertion device) | MeV |
| Momentum compaction               | $1.45 \times 10^{-3}$ |       |
| Damping partition (H / V / L)     | 1.82 / 1.0 / 1.18 |       |
| Damping time (H / V / L)          | 13.37 / 24.35 / 20.66 | ms   |
| Main RF voltage                   | 2.15      | MV    |

Figure 3
Beam distribution at the watching point with 100000 particles prepared for examination of intrinsic resolution. (a) TDC off; (b) TDC on.
0.037 mm on the x axis and 0.022 mm on the y axis, which are explained by \( \sigma_x \simeq R_{11}^\delta \sigma_{y1} + R_{12}^\delta \sigma_{y2} \) and \( \sigma_y \simeq R_{33}^\delta \sigma_{y3} + R_{34}^\delta \sigma_{y4} \). When the TDC was on, the x axis was not affected, but five resolved distributions appeared on the y axis [Fig. 3(b)]. The effective length on the y axis increased from 0.13 mm to 5.95 mm due to \( y \simeq R_{44}^\delta \varepsilon_z \) whereas the standard deviations of the Gaussian peaks did not change. These processes allow clear resolution of the five Gaussian peaks [Fig. 4(c)]. From the revealed Gaussian peaks with the use of a line distribution on the longitudinal plane, we define the intrinsic resolution on an axis as \( R_i = (\text{distance between adjacent Gaussian peak}) / \) (standard deviation of a Gaussian peak). \( R_i \) increases with increase in the clarity of distinction of the Gaussian peak on an axis. PAL-4GSR has \( R_i = 6.69 \) on the x axis and \( R_i = 64.68 \) on the y axis. The dispersion bump (for \( \delta-x \) correlation) increases and the voltage of the TDC increases (for \( z-y \) correlation), so the resolution can be increased. Adjustment of dispersion bumps is constrained by lattice requirements, but the voltage of the TDC can be increased further without affecting lattice requirements and we can expect much better resolution than is currently achieved.

4. Application on PAL-4GSR

A Gaussian bunch of 100000 particles in an equilibrium state was generated for the six-dimensional phase space with the round-beam mode. It had 58 pm emittance in both horizontal and vertical phase spaces. It should be mentioned that, for simplicity, distributed coupling errors are considered along the ring except for the region from the TDC and watching point to generate round beam. With a main RF voltage of 2.15 MV, its longitudinal distribution had \( \sigma_y = 0.00108 \) and \( \sigma_z = 7.677 \) mm (Table 2). For a TDC, a voltage of 4.5 MV and a frequency of 750 MHz were also used.

4.1. Longitudinal emittance measurement

The longitudinal emittance can be written with the standard deviation as

\[
\varepsilon_z = \sigma_z \sigma_\delta. \tag{5}
\]

Here, using equation (4), the standard deviations \( \sigma_z \) and \( \sigma_\delta \) can be approximately converted to

\[
\sigma_z \simeq \eta_z \sigma_\delta \tag{6}
\]

and

\[
\sigma_\delta \simeq R_{44}^\delta \varepsilon_z, \tag{7}
\]

respectively. Therefore, measurements of \( \sigma_z \) and \( \sigma_\delta \) directly lead to estimates of longitudinal emittance. The generated Gaussian bunch is deflected at the TDC. After a \( \pi/2 \) phase advance (at a watching point), the bunch’s projection on the \( x-y \) plane has a clear Gaussian distribution [Fig. 5(b)], with \( \sigma_x = 0.197 \) mm and \( \sigma_y = 0.922 \) mm. From these values, re-projection using equation (4) gives \( \sigma_z = 1.096 \times 10^{-3} \) and \( \sigma_x = 7.680 \) mm, which have 1.46% and 0.04%, respectively, error relative to the original values. As a result, the longitudinal emittance from the measurement is calculated to be \( \varepsilon_z = 8.417 \times 10^{-6} \) m, which is a 1.52% error relative to the original value. The original longitudinal profile at the TDC and the profile (Fig. 6) were obtained from re-projection using equation (4).

4.2. Measurement of the longitudinal phase space profile with instability

Beam manipulation in the longitudinal phase can be used to generate coherent radiation (Ratner & Chao, 2010) and beam dynamics in the longitudinal phase space to enable exploration of a new injection scheme (Kim et al., 2019; Aiba et al., 2015; Jiang et al., 2016; Jiang & Xu, 2018; Kuske et al., 2020). These goals invoke a need to measure the longitudinal beam profile. To generate a special shape in the longitudinal phase space, instabilities were deliberately induced by using wake-field data – here the impedance data of APS (Chae, 2003, 2007; Lindberg & Blednykh, 2015). However, PAL-4GSR and APS have different characteristics such as circumference (PAL-4GSR

| Parameter                  | Value | Unit |
|----------------------------|-------|------|
| Horizontal emittance       | 58    | pm   |
| Vertical emittance         | 58    | pm   |
| Energy spread (r.m.s.)     | 0.00108| –    |
| Bunch length (r.m.s.)      | 7.677 | mm   |

Table 2: Particle distribution at the equilibrium.

Figure 4: Density distribution on the x and y axis for the beam distribution shown in Fig. 3. (a) Density on the x axis when the TDC is on or off, (b) density on the y axis when the TDC is off, and (c) density on the y axis when the TDC is on.
4GSR: 570 m; APS: 1100 m), nominal energy (PAL-4GSR: 3 GeV; APS: 7 GeV), so use of these data can invoke instabilities in PAL-4GSR. We first estimated the current threshold $I_{\text{threshold}}$ of the strong instability by following Boussard’s criterion (Boussard, 1975),

$$I_{\text{threshold}} = \left( \frac{2\pi}{\alpha_c \sigma_z E \sigma_\phi^2} \right)^{1/2} c T_0 \left| Z_k \right| / n,$$

where $\alpha_c$ is the momentum compaction, $\sigma_z$ is the equilibrium bunch length, $\sigma_\phi$ is the equilibrium relative energy spread, $c$ is the speed of light, $T_0$ is the revolution time, and $|Z_k/n|$ is the effective longitudinal impedance. This conservative estimate gives $I_{\text{threshold}} \approx 0.37$ mA; therefore we used a single bunch current of 7.7 mA (or single bunch charge of 15 nC) which is sufficiently high above the estimated threshold. Including the impedance data, a tracking simulation was conducted using a Gaussian bunch of 100000 particles in the equilibrium state. Oscillations of r.m.s. bunch length and r.m.s. energy spread along a number of turns show that both quantities increased rapidly after tracking started, reached their maximum within 2000 turns and eventually converged to a new equilibrium at ~10000 turns (Fig. 7). The new equilibrium with the impedance data has 1.3 times larger bunch length and 1.8 times larger energy spread, compared with the original equilibrium. Those results imply that strong instability was driven well.

We next examined longitudinal beam profiles at 10000 turns (Fig. 8). After the kick of the TDC was applied, the longitudinal phase space was projected to the $x$–$y$ plane. The central beam distribution split up and the outer beam distribution seems to have a spiral shape. Also, the center of the bunch was moved to ~0.3 mm on the $x$ axis. The overlap of the original longitudinal profile [Fig. 8(a)] and re-projection from the $x$–$y$ plane [Fig. 8(b)] using equation (4) agreed well (Fig. 9).

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5. Conclusion

We have described a novel scheme to measure the emittance and phase space profile in the longitudinal plane by using correlations between time and the vertical coordinate, and between energy and the horizontal coordinate. A large dispersion bump has a strong correlation with energy and the horizontal coordinate, and the crab cavity has a strong correlation with time and the vertical coordinate. As a result, longitudinal emittance was estimated with <1.52% error in the PAL-4GSR lattice and micro-bunching instability was observed at the synchrotron radiation source point. This longitudinal profile measurement scheme will help to guide the manipulation of beams in longitudinal phase space.

APPENDIX A

Definitions of each matrix element of equation (2)

\[
R_{11} = \left( \frac{\beta_{x2}}{\beta_{x1}} \right)^{1/2} \cos \psi_x + \alpha_{x1} \sin \psi_x, \\
R_{12} = \left( \frac{\beta_{x1}}{\beta_{x2}} \right)^{1/2} \sin \psi_x, \\
R_{21} = -\frac{1}{(\beta_{x1} \beta_{x2})^{1/2}} \left[ (1 + \alpha_{x1} \alpha_{x2}) \sin \psi_x - (\alpha_{x1} - \alpha_{x2}) \cos \psi_x \right], \\
R_{22} = \left( \frac{\beta_{x1}}{\beta_{x2}} \right)^{1/2} \cos \psi_x - \alpha_{x2} \sin \psi_x, \\
R_{33} = \left( \frac{\beta_{y1}}{\beta_{y2}} \right)^{1/2} \cos \psi_y - \alpha_{y1} \sin \psi_y, \\
R_{34} = \left( \frac{\beta_{y1} \beta_{y2}}{\beta_{y1} \beta_{y2}} \right)^{1/2} \sin \psi_y. \\
\]

\[
R_{43} = -\frac{1}{(\beta_{y1} \beta_{y2})^{1/2}} \left[ (1 + \alpha_{y1} \alpha_{y2}) \sin \psi_y - (\alpha_{y1} - \alpha_{y2}) \cos \psi_y \right], \\
R_{44} = \left( \frac{\beta_{y1}}{\beta_{y2}} \right)^{1/2} \cos \psi_y - \alpha_{y2} \sin \psi_y, \\
A = R_{21} \eta_2 - R_{11} \eta_1 + \eta_1', \\
B = -R_{12} \eta_1' + R_{22} \eta_2 - \eta_1, \\
C = -\int_{\xi_1}^{\xi_2} \frac{\eta(s)}{\rho(s)} \, ds.
\]
$\alpha$, $\beta$ are typical beta functions, $\eta$, $\eta'$ are dispersion functions, with corresponding subscript. $\psi_x$ and $\psi_y$ are, respectively, the horizontal and vertical phase advances between positions 1 and 2.

Acknowledgements

We thank G.-R. Hahn and T. Ha (PAL) for providing helpful information and many useful discussions.

Funding information

Funding for this research was provided by: National Research Foundation of Korea (grant No. NRF-2019R1C1C1003412; grant No. NRF-2019R1A2C1004862).

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