Friction of water on graphene and hexagonal boron Nitride from \textit{ab initio} methods: very different slippage despite very similar interface structures

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Friction is one of the main sources of dissipation at liquid water/solid interfaces. Despite recent progress, a detailed understanding of water/solid friction in connection with the structure and energetics of the solid surface is lacking. Here we show for the first time that \textit{ab initio} molecular dynamics can be used to unravel the connection between the structure of nanoscale water and friction for liquid water in contact with graphene and with hexagonal boron nitride. We find that whilst the interface presents a very similar structure between the two sheets, the friction coefficient on boron nitride is \(\approx 3\) times larger than that on graphene. This comes about because of the greater corrugation of the energy landscape on boron nitride arising from specific electronic structure effects. We discuss how a subtle dependence of the friction on the atomistic details of a surface, that is not related to its wetting properties, may have a significant impact on the transport of water at the nanoscale, with implications for the development of membranes for desalination and for osmotic power harvesting.

Nanofluidics is an exciting field that offers alternative and sustainable solutions to problems relating to energy conversion, water filtration and desalination [1–9]. Miniaturization towards nanofluidic devices inevitably leads to an enhanced influence of surface and interface properties as opposed to those of the bulk. Friction is the most important interface property that limits fluid transport at the nanoscale, and its understanding is therefore crucial for the design of more efficient membranes, nanotubes and pores that exhibit low liquid/solid friction. The behavior of liquid flow at scales on the order of a few tens of nanometres departs from continuum fluid dynamics and desirable transport properties emerge at such small scales [10]. For instance, carbon nanotubes have a very high water permeability as compared to the prediction of macroscopic fluid dynamics [2]. Further, a vanishing friction has been found, giving rise to superlubric behavior of water chains inside tubes of sub-nanometre radii [11].

Besides carbon, boron nitride (BN) nanostructures have recently been explored for the development of nanofluidic devices for fast water transport and efficient power generation [1] [12] [13]. Recent interest has been fueled by the demonstration that salinity concentration gradients across BN nanotube membranes can lead to the generation of very large electric currents [1]. It has also very recently been shown that there is a very large inter-layer friction between in multiwalled BN nanotubes [14], as opposed to the superlubric behavior of the (homopolar) carbon nanotubes [15]. This suggests that the frictional properties of BN and C nanostructures might be quite different. However, to the best of our knowledge there has been no attempt to measure or compute the friction of water at the interface with BN sheets or nanotubes. Given that \textit{ab initio} results have shown very similar contact angles of water droplets on graphene and BN sheets [19], it remains to be seen if transport properties on these two systems are also similar.

The rise of the atomic force microscope and the surface force apparatus has advanced our understanding of nanoscale liquid/solid friction substantially [17]. Yet, it remains extremely hard to relate friction and dynamics to structure and wetting of solid surfaces from experiment. This is especially true for the case of graphene where there is even controversy over the water contact angle (see e.g. Refs. [18] [19]). Molecular simulations, and especially force field molecular dynamics, have proved extremely useful in investigating structural and dynamical properties of confined liquids elucidating molecular level information that is challenging for experiments to obtain. Because of the dependence of simulation results on the parametrization of force fields, it is interesting to investigate the dynamics of interfacial water using electronic structure methods so that two different materi-
als such as graphene and BN can be compared on an equal footing. Accordingly, \textit{ab initio} molecular dynamics (AIMD) offers an interesting alternative that has been widely used to study complex liquid/solid interfaces (see e.g. Refs. \cite{10, 20, 21}). Although transport properties in liquids have been computed before using AIMD (see e.g. Refs. \cite{22, 24}), we show for the first time that it is possible to compute a converged friction coefficient from AIMD.

In this work we compare the structure and dynamics of water in contact with BN and carbon nanostructures from AIMD. Specifically, we study liquid water in contact with graphene and hexagonal BN sheets, which is relevant to understanding flow at membranes based on these materials and also inside large nanotubes \cite{23}. We find a striking similarity between the structure of water in contact with the two sheets. Nevertheless, there is a three-fold increase in the friction coefficient on BN because of a more corrugated free energy surface on BN compared to graphene. This work illustrates the complexity of nanoscale friction where subtle electronic effects, with no detectable consequences on the structure of the liquid, may however have a dramatic impact on water transport at the nanoscale.

We performed a series of extensive AIMD simulations of a thin liquid water film on graphene and on a single layer of hexagonal BN. Full details of the computational set-up can be found in the Supporting Information (SI). However, the key features are that we used the CP2K \cite{26} code to perform AIMD simulations in the Born-Oppenheimer approximation with the electronic structure computed at the density functional theory (DFT) level using the optB88-vdW exchange-correlation functional \cite{27, 28}. The optB88-vdW density functional has been shown to predict accurate interlayer binding and interlayer distances in graphite and bulk hexagonal BN \cite{29}, to give a good description of the structure of bulk liquid water \cite{30} and also to correctly describe the relative stability of water-ice structures on metals compared to the bulk ice lattice energy \cite{31}. The water/graphene and water/BN sheets have been modelled using $6 \times 10$ orthorhombic cells about $25 \times 25 \times 25$ Å$^3$ wide, with $\approx 20$ Å thick liquid water films. There is a vacuum gap between the liquid-vacuum interface and the next periodic image of $\approx 15$ Å. Each film contains 400 water molecules and in total each system consists of 1440 atoms. Upon these systems we performed 40 ps long AIMD simulations with the last 35 ps of each trajectory used for analysis. As an illustration snapshots from the AIMD simulations for the water/graphene and water/BN interfaces are shown in Fig. 1(c) and (d), respectively. The AIMD simulations are in the canonical ensemble close to room temperature (330 K). We also performed a number of additional AIMD and force field MD simulations to explore the sensitivity of our results to the use of a different ensemble and to issues such as finite size effects, different initial conditions and time scales. Overall, the results of these tests, which can be found in the SI, agree with the results presented herein.

![FIG. 1. Structure of the liquid water film on graphene (GRA) and a single sheet of hexagonal BN. Average density profile $\langle \rho \rangle$ (a) and number of hydrogen bonds (H-bonds/H$_2$O) (b) as a function of the height from the sheet. In (b) the geometric criterion from Luzar and Chandler was used to define a H-bond. Snapshots of the liquid film on GRA (c) and on BN (d). In (c) and (d) O and H atoms are coloured in red and white, while C atoms are in light blue, and B and N atoms are in pink and purple, respectively. The liquid film structure is essentially the same on both sheets, only on BN the film is slightly thinner because the BN unit cell is $\approx 3.5\%$ larger than that of graphene.](image-url)

We begin our analysis by illustrating in Fig. 1(a) the planar average density profile $\langle \rho \rangle$ as a function of the height from the sheets. The graphene and BN sheets exhibit oscillations in the heights of the atoms within them of up to 1.2 Å. To account for this, we compute the height of an atom in the liquid water overlay as the height difference to the closest atom in the sheet. By computing the density profile in this way we fully account for the layering of the liquid film, which would otherwise be partially hidden behind the oscillations of the sheets. The two density profiles on graphene and BN overlap for most of the film height, which is the first signature of the apparent similarity of the structure of liquid water on the two sheets. Perturbation from the bulk liquid induced by the surface is most significant within the first 10 Å of the surface. This is consistent with previous reports on liquid water/solid interfaces (see e.g. Refs. \cite{20, 21, 33, 34}), which extends in this case to about 8 Å from the sheets. Within this region there are two evident peaks for each of the two density profiles. The first at a height of about 3.0 Å hits a density maximum of $\approx 3.7$ g/cm$^3$. After this first peak there is a depletion of water with a minimum at about 4.5 Å with a density of 0.4 g/cm$^3$. We define the contact layer as the region delimited by this minimum in the density profile. At $\approx 6.0$ Å the second peak appears with a density of $\approx 2$ g/cm$^3$. Further away from the sheets, density oscillations are gradually suppressed and the density of liquid water is recovered with an average
value of $1.12 \pm 0.16 \text{ g/cm}^3$. Finally, the density decays as it is characteristic of the liquid-vapor interface. The decay in the density on BN starts off at about 17 Å, slightly before than on graphene simply because the BN unit cell is $\approx 3.5\%$ larger.

As further confirmation of the striking similarity between the structure of liquid water on graphene and BN, we compare the profile of the average number of H-bonds per molecule, $\langle \text{H-bonds/H}_2\text{O} \rangle$ in Fig. 1(b). Also in this case the two curves essentially lie on top of each other for all of the film height apart from the liquid-vapour interface region. The steep increase in the (H-bonds/H$_2$O) starting at about 2 Å shows that already in the contact layer water molecules engage in a large number of H-bonds of $\approx 3$ H$_2$O. Shortly after this initial increase, there is a drop to $\approx 2.5$ H-bonds/H$_2$O corresponding to the depletion region around 4.5 Å from the sheet. The pronounced fluctuations in the number of water molecules in this region partly penalizes H-bonding with neighboring waters. After the depletion region, at a height of 5 Å, the number the (H-bonds/H$_2$O) rises to the bulk value of $\approx 3.5$. It remains constant until the liquid-vapour region is approached, at a height of 17 Å, where there is a rapid decay to zero in the (H-bonds/H$_2$O) within 3 to 4 Å. Finally, other structural characteristics of the two systems exhibit striking similarities, such as the orientations of the water molecules within the films (see Fig. S2 in the SI).

Having compared the structure of liquid water on the two sheets we now turn our discussion to investigate its dynamics. Specifically, we focus on the friction coefficient $\lambda$, defined as the ratio between the friction force parallel to the sheet $F_p$ per unit area ($A$) and $v_{\text{slip}}$, the velocity jump at the interface [10], namely $\lambda = F_p/(A v_{\text{slip}})$. In the framework of linear response theory, $\lambda$ can be obtained from the equilibrium fluctuations of the friction force, using a Green-Kubo relation [36, 37]:

$$\lambda = \lim_{t \to \infty} \lambda_{\text{GK}}(t),$$  \hspace{1cm} (1)

with

$$\lambda_{\text{GK}}(t) = \frac{1}{2 k_B T} \int_0^t \langle F_p(t') \cdot F_p(0) \rangle \, dt'$$  \hspace{1cm} (2)

where $k_B$ is the Boltzmann constant, $T$ the temperature and the factor of $1/2$ comes from the averaging over the two spatial dimensions parallel to the sheets. We show in Fig. 2 $\lambda_{\text{GK}}(t)$ for the case of water on graphene and on BN, which for sufficiently long time intervals (here approximately $> 0.3$ ps) plateaus to the value of $\lambda$. The key result is that the friction coefficients on the two sheets differ significantly, with the friction on BN being approximately 3 times larger than on graphene. Specifically, while $\lambda = (9.6 \pm 2.0) \times 10^4 \text{ N s m}^{-3}$ for graphene, we obtain a value on BN of $\lambda = (30.0 \pm 5.4) \times 10^4 \text{ N s m}^{-3}$. A number of tests using both AIMD and force field MD, ensured that our results on the friction coefficients are converged and that the increase of about three times in the friction on BN compared to graphene is consistently observed, regardless of the type of ensemble used, time scales, or different system sizes. The results of these tests are presented in Fig. S3 in the SI.

Whilst liquid/solid friction is the relevant microscopic property that quantifies the dynamics of a fluid at the nanoscale, a length scale characteristic of the flow is often measured experimentally. This is the so-called slip length $b$, defined as the distance relative to the surface where the linear extrapolation of the tangential flow velocity vanishes. We can relate the slip length $b$ to the friction coefficient via the shear viscosity of bulk liquid water $\eta$: $b = \eta/\lambda$ [10]. Using the experimental bulk water viscosity $\eta = 10^{-3}$ Pa s, the corresponding slip lengths for graphene and BN are $10.4 \pm 2.2$ and $3.3 \pm 0.6$ nm, respectively. Overall water slippage on graphene and BN is characteristic of hydrophobic surfaces with a low friction coefficient, while on hydrophilic surfaces such as mica, silicon or graphene oxide slippage is significantly inhibited with sub-nm slip lengths [38, 39].

![Fig. 2. Comparison between the Green-Kubo estimate of the friction coefficient of liquid water on graphene (GRA) and on BN. The shaded areas represent the uncertainties obtained by performing a block average. The friction coefficient $\lambda$ is given by the plateau value at long times. There is an evident increase in the friction coefficient on BN.](image)
has been used previously to understand water slippage on model MgO surfaces. 

Fig. 3 illustrates the free energy profiles resulting from this analysis. We notice the very small energy scale within k_BT at room temperature indicating a mobile contact layer. Although, the average liquid structures in the two systems are very similar, the free energy profiles for the motion of water in the contact layer exhibit some clear differences. First, the free energy minimum on graphene is around the hollow site with the maximum around the top-C site, in agreement with previous work. The minimum on BN is for the oxygen to sit around the B-site, as well as on the hollow site, while the maximum is on the N site. Second, and more importantly, the BN free energy profile (Fig. 3(b)) is more corrugated than that of graphene: the maximum corrugation of the free energy is only 13 meV on graphene, but it is 21 meV on BN. Although we are discussing very small energies, this ≈ 60% increase in the corrugation is observed consistently in all our various AIMD simulations of these systems. Indeed, the corrugation is already converged if the free energy profile is extracted from half the AIMD trajectory, as opposed to the full trajectory (see Fig. S5). As we now discuss, this increased corrugation is the main reason for the observed increase in the friction coefficient on BN.

It is interesting that such small energy differences, less than 10 meV can contribute to a three fold increase in the friction coefficient and it is worth looking into this more in detail. It is known that the leading term in the friction depends quadratically on the corrugation of the potential energy surface felt by the water in the contact layer ∆V, such that λ ∼ ∆V^2 (see e.g. [7, 41]). We can approximate the corrugation of the potential energy ∆V with the corrugation in ∆G as obtained from the maximum value in free energy profiles in Fig. 3, such that λ ∼ ∆G^2. To test the validity of this scaling relation we computed the ratio between the friction of water on BN and on graphene, λ_{BN}/λ_{GRA} and compared it with the ratio between the square of the free energy extracted from Figs. 3(a) and (b). From the ratio between the friction coefficients we obtain λ_{BN}/λ_{GRA} = 3.1 ± 0.8. The corrugation of the free energy on BN is 21 meV, while it is 13 meV on graphene, such that the ratio (∆G_{BN}/∆G_{GRA})^2 ≈ 2.6, is within the error of the ratio between the two values of the friction.

The free energy corrugation depends on the atomic and electronic structure of the surface and on the H-bonds that form at a specific interface. It will differ but be related to the monomer potential energy surface. By performing an extensive series of calculations (about 4000 wave function optimizations per sheet) we mapped the potential energy surface of a water monomer on the sheets (see Fig. S1), to explore if the potential of a water monomer on BN is more corrugated than that on graphene. This confirms that the free energy of the water contact layer on BN is more corrugated than that on graphene because the potential of the water monomer is also more corrugated.

From the analysis of the different structures of a water monomer on the two sheets, we have identified the main sites that give rise to the most and least stable configurations of water on graphene and BN. The most stable structure on graphene is for water on the center of the hexagon with its dipole pointing down towards the sheet (Fig. 3(c)). On BN water preferentially adsorbs in the center of the hexagon with the dipole moment parallel to the sheet and with one of the O–H bonds pointing towards the N atom (Fig. 3(e)). Upon considering water monomer adsorption at less favorable sites (see Figs. 3(d) and (f)) we find that indeed the potential energy surface of the water monomer on BN is more corrugated than that on graphene (see Table S1). To understand the reason for the different corrugation between the two sheets, we performed a decomposition of the interaction energies of several water structures on the sheets at the more stable sites (on the center of the hexagon of graphene and BN) and at less stable sites (on the top-C and top-N site), as shown in Table S1. Although there is a certain level of arbitrariness to most decomposition schemes,
we have used an established approach to gain qualitative and semi-quantitative insight into our adsorption systems (see e.g. Refs. [29, 31]). This analysis reveals that van der Waals dispersion forces and local-correlation effects do not contribute to the corrugation of the graphene and BN sheets. On the other hand, the interactions arising from exchange, electrostatic and electron kinetic energy terms are overall more pronounced on BN and provide the reason for the increased corrugation, and thus for the 3-fold increase in the friction. Finally, we note that even though very small energy differences are being reported for the corrugation of the free energy profile, our AIMD simulations are long enough that the free energy profiles are converged even if they are extracted over half the trajectory (see Fig. S5). Also, these differences are robust with respect to the accuracy of the underlying potential energy surface (see Fig. S1) and they are consistent with the monomer interaction energies computed in Table S1 using different codes and exchange-correlation functionals.

Since this is the first AIMD study of water slippage at either of the two sheets examined, we wish to compare our results with the existing literature. In the absence of experiments on graphene or BN we compare our results to those obtained from atomic force microscopy measurements of water droplets on atomically smooth highly ordered pyrolytic graphite, which have given slip lengths of between 8 and 12 nm [29, 32], in good agreement with our value for the slip length of 10.4 ± 2.2 nm. Although on graphene water transport may differ from that on graphite due to e.g. screening effects that may influence the binding on the two systems [13], we do not expect the friction to change between graphene and graphite by more than a few percent.

Compared to previous simulation studies, we notice that there is some uncertainty over the slippage of water on graphene obtained from force field MD, with values for the slip length between 1 and 80 nm [14], and our AIMD result falls in this somewhat large range. The value of the friction on graphene obtained from our force field MD is \(3 \times 10^4\) N m^{-3} (see Fig. S3(b)), about 3 times smaller than our AIMD value of \((9.6 \pm 2.0) \times 10^4\) N m^{-3}. This is because the optB88-vdW functional predicts a larger corrugation of the free energy compared to the force field used [15](see Fig. S4). Since optB88-vdW overestimates the absolute adsorption energy of a water monomer on graphene when compared to benchmark diffusion Monte Carlo and Random Phase Approximation results [16], we cannot expect optB88-vdW to capture the corrugation of the free energy with absolute precision. However, as explained earlier, because this functional successfully captures various other properties of water, graphite, BN and water at interfaces we expect it to predict the correct relative water/graphene and water/BN interaction strengths and hence the correct increase in the friction on BN. Since the increase in friction is not captured by force field molecular dynamics (see Fig. S3(b)), the findings here stress the importance of accounting for electronic structure effects when investigating transport properties at complex liquid/solid interfaces. Nevertheless, it is possible that improving the description of the force fields to include polarizable models and partial charges on B and N may reproduce the observed friction increase. For instance, it has been found that including polarization effects in force field molecular dynamics studies has an effect on the diffusion of liquid water on charged graphene [31].

Finally, there has been increasing interest in connecting wetting properties to the friction coefficient (see e.g. Ref. [32]) and a relation between the slip length and the contact angle has been found to hold for a wide number of liquid/solid interfaces. Here we have seen that the structure of liquid water on graphene and on BN is strikingly similar and previous ab initio work reported also contact angles of 86° and 87° on graphene and BN, respectively [14]. Yet, friction is about three times larger on BN, highlighting that a simple dependence on the wetting properties cannot be established for these two systems.

Instead, we have demonstrated a dependence of the friction on the free energy of the water contact layer. In systems like graphene and BN, where the corrugation of the potential felt by the water is not directly proportional to the water/solid interaction strength, the free energy profile provides a closer estimate of the potential energy landscape corrugation. Possible other examples are carbon nanotubes, which like graphene, have been shown to depart from the scaling law that relates the friction to the water contact angle [14]; and most likely BN nanotubes and other van der Waals layered materials [47]. With the aim of designing nanofluidic devices which exhibit frictionless fluid transport, materials may be engineered to favor a smooth potential energy landscape independently of the fluid/solid interaction strength. In this manner for instance, the friction may be tailored whilst maintaining the same wetting properties. We have shown that because of electronic structure effects, friction is larger on BN. Limiting the magnitude of such interactions between the liquid and the substrate using for instance homopolar surfaces and avoiding the presence of H-bonds is beneficial for the design of smooth interfaces. Further, compressive or tensile stress can be applied to a substrate to favor a smooth contact layer [38].

In conclusion, we have reported on extensive ab initio molecular dynamics studies of liquid water on graphene and BN. In so doing we have tried to bridge the gap between the molecular structure and energetics of water on layered materials and the complex transport of water at the nanoscale fully from ab initio methods. A comparison between the two systems reveals that while the structure of the liquid film is very similar, slight differences in the water contact layer not related to the wetting properties of the interfaces give rise to a remarkably different
water slippage on the two sheets. The three-fold friction increase on BN is induced by a larger corrugation of the energy landscape compared to graphene, because of more pronounced electrostatic and exchange interactions. Overall, this work paves the way for the study of transport properties in yet more complex liquid water/solid interfaces using ab initio methods. For example, systems where water is liable to dissociate or where ions, defects, or external electric fields are present could all be examined. We also hope that our work will stimulate the study of nanoscale water friction on BN-nanostructures and other layered materials using e.g. atomic force microscopy [39].

SUPPLEMENTARY INFORMATION

Further computational details and tests on the structure, energetics and friction coefficient of the water/graphene and water/BN interfaces.

ACKNOWLEDGEMENTS

We are grateful to Lyderic Bocquet for encouraging us to carry out this work. The early stages of this work were supported by the FP7 Marie Curie Actions of the European Commission, via the Initial Training Network SMALL (MCITN-238804). LJ is supported by the French Ministry of Defense through the project DGA ERE number 2013.60.0013.00.470.75.01, and by the “labex iMUST” through the “mobilité out” program. A. M. is supported by the European Research Council (HeteroIce project) and the Royal Society through a Wolfson Merit Award. We are also grateful for computational resources to the London Centre for Nanotechnology and to the UK’s HPC Materials Chemistry Consortium, which is funded by EPSRC (EP/F067496), and to the UKCP consortium, EP/F036884/1 for access to HECToR and Archer.

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