Abstract

Background: Developmental dysplasia of the hip (DDH) can be detected with ultrasonography (USG) images. However, the accuracy of this method is dependent on the skill of the radiologist. Radiologists measure the hip joint angles without computer-based diagnostic systems. This causes mistakes in the diagnosis of DDH.

Objectives: In this study, we aimed to automate segmentation of DDH ultrasound images in order to make it convenient for radiologic diagnosis by this recommended system.

Materials and Methods: This experiment consisted of several steps, in which pure DDH and various noise-added images were formed. Then, seven different filters (mean, median, Gaussian, Wiener, Perona and Malik, Lee, and Frost) were applied to the images, and the output images were evaluated. The study initially evaluated the filter implementations on the pure DDH images. Then, three different noise functions, speckle, salt and pepper, and Gaussian, were applied to the images and the noisy images were filtered. In the last part, the peak signal to noise ratio (PSNR) and mean square error (MSE) values of the filtered images were evaluated. PSNR and MSE distortion measurements were applied to determine the image qualities of the original image and the output image. As a result, the differences in the results of different noise removal filters were observed.

Results: The best results of PSNR values obtained in filtering were: Wiener (43.49), Perona and Malik (27.68), median (40.60) and Lee (35.35) for the noise functions of raw images, Gaussian noise added, salt and pepper noise added and speckle noise added images, respectively. After the segmentation process, it was seen that applying filtering to DDH USG images had low influence. We correctly segmented the ilium zone with the active contour model.

Conclusion: Various filters are needed to improve the image quality. In this study, seven different filters were implemented and investigated on both noisy and noise-free images.

Keywords: Ultrasonography, Image Processing, Developmental Dysplasia of the Hip, Filtering

1. Background

Developmental dysplasia of the hip (DDH) or dislocation of the hip is a structural defect, which results in incompatibility between the femoral head and the acetabulum. The prevalence rate of the disease has been determined as 1/3000 in the world but is higher in Japan and in the Mediterranean Basin (1). DDH can be treated successfully with early diagnosis. Delay in diagnosis and treatment can cause the extremities (limbs) to shorten, and claudication and restricted movement disorders, which can lead to functional disabilities. If, it is diagnosed in the neonatal period, the success rate of the treatment is 96% in infants, who can achieve anatomically and radiologically normal development following the treatments (2). In children who have reached the age of walking, there is no chance of conservative treatment and surgery is the only course of action. It is unfortunately impossible to get successful results with surgical treatment in all patients. Even if the surgery is successful, the side effects are too great to be ignored (3).

Determining the incidence of DDH requires examining the abnormal situations where there are differences in the hips, and even then the successful detection of a DDH incidence will depend on the method selected, the level of knowledge of the examiner and the community. The incidence rate based on examining approximately 1000 births was reported to be in the 3 - 4% range. Compared to physical examination, ultrasonography (USG) imaging studies have reported better detection and higher incidence rates (4).

Hip developmental disorders can be successfully de-
tected using USG, and following the detection of the disease, staging and treatment can be planned. Technically, the methods of Graf, Harcke, and Terjes are used (5). USG imaging has become one of the most preferred imaging techniques in today’s medical practices, and therefore, is also widely used in the detection of DDH. This wide use is because USG is inexpensive, easily available and comparatively safe to the patients, as well as the operators. It is estimated that one out of every four medical diagnostic image studies in the world involves ultrasonic techniques (5). In addition, because the diagnosis of DDH is carried out in the newborn period, the use of USG in infants also prevents exposure to radiation.

The Graf method is commonly used in the diagnosis of DDH with USG images. Graf is a morphological approach where the anatomical features are assessed in a single image of the hip. To use this method, first, the baby is laid on its side and the transducer is placed parallel to the axis of the body with the specific anatomic landmarks (femoral head and acetabulum). Then, the image is displayed in the standard plane and the morphology is determined by measuring the angles of the hip joint (α and β), as shown in Figure 1. However, the low image quality, in general, makes it difficult for the radiologist to determine the hip joint angles.

The presence of noise in the USG images, leads to image quality degradation and reduction in the ability to achieve successful detection (6). In other words, processing USG images is a difficult and challenging task. Therefore, in order to facilitate image processing, pre-processing filters should be applied to the images. Improving the images by applying filters makes the segmentation process more effective.

There are a few studies regarding computer-aided diagnosis of developmental dysplasia of the hip. Luis-Garcia and Alberola-Lopez studied computer-aided diagnosis of developmental dysplasia of the hip. They tried to segment the acetabulum and femur region from USG images (7-9). Their first work (7) was based on the dynamic shape priors method for segmentation of the nonlinear structure tensor in the tensor domain. They proposed dynamically constructing the shape prior, using the anatomical knowledge as well as the segmentation flow itself. In their study, preliminary data on real images showed promising results (7). In 2006, they presented a segmentation method for the hip joint from three-dimensional (3D) ultrasound data. The Kullback-Leibler distance measurement was used as an intrinsic dissimilarity measure; the energy minimization is performed by estimating the optimal parameters of the sphere and paraboloid that best approximate the femoral head and acetabulum, respectively. Experimental results in this study, over several data volumes, showed this approach to be capable of successfully approximating the anatomy of the hip joint using simple geometrical surfaces (8). In 2007, they presented a novel technique for the analysis of ultrasound images, based on the local estimation of parameter σ of the Rayleigh distribution, which is assumed to model the ultrasound signal. It has been shown that the transformation of the original ultrasound image into the local estimator increases the separability between different regions of interest in the hip joint ultrasound images (9). Han-Yong et al. designed and implemented a computer-aided system for treatment of this disease. In this system, they used a mixture-based partial-volume (PV) algorithm to perform bone segmentation on the patient’s computed tomography (CT) or magnetic resonance imaging (MRI) image, then, using 3D reconstruction and display of the segmented image, they easily obtained the quantitative measurement of the acetabular index (AI) and the center-edge angle (CEA), which helped in the clinic diagnosis and treatment (10).

Generally, in diagnosis of dysplasia of the hip joint, the assessment of USG images is performed by the radiologist or operator in real-time. However, in some situations, the real-time images are saved for further assessments. In this study, the saved images were used for researching the filtering effects. On the other hand, this filtering application can be implemented online as well. In our future work, we are planning to improve the online automatic diagnosis system for determining DDH abnormalities on USG devices.

This study is part of the computer-aided diagnostic system of DDH diseases. As a pre-processing of the segmentation of USG images, the effects of various filters were measured by applying them to these images. In our study, seven different filters were applied; mean, median, Gaussian, Wiener, Perona and Malik, Lee and Frost, which are widely known and cited in the literature for their ability to obtain better quality USG DDH images. In addition, various noises were added (speckle, salt and pepper, and Gaussian) to the raw DDH USG images. Then, the peak signal to noise ratio (PSNR) and mean square error (MSE) were measured in order to evaluate the effect of the filters on segmentation. The last stage of our study was testing images on the USG images segmentation method by applying to the active contour method. This segmentation process was aimed to investigate the ilium zone.

2. Objectives

In this study, we aimed for the automatic segmentation of DDH ultrasound images, in order that radiologists can gain convenience in diagnosis by using this recommended system.
3. Materials and Methods

The raw USG images used in this research were acquired from one device (Toshiba Aplio 400) by one radiologist in the Selcuk university, faculty of medicine, radiology department. These acquired images can differ depending on the probe position and the operator skill. To eliminate the differences caused by having different USG operators, the study uses only one radiologist. The radiologist captures the USG images when he decides to get the best image that can be used for diagnosis of DDH.

The USG images acquired were from infants ranging from 0 - 3 month old (ten anatomically normal babies were randomly chosen), who were laid down laterally onto the table, which had special adaptions used to grasp the baby from both sides in order to keep them still while capturing the image.

This experiment consisted of several steps, in which pure DDH and various noise-added images were formed. Then seven different filters (mean, median, Gaussian, Wiener, Perona and Malik, Lee and Frost) were applied to the images, and finally, the output images were evaluated. The filters used, which are known in the literature, are described in the appendix.

The study initially evaluated the filter implementations on the pure DDH images. Then, three different noise functions; speckle, salt and pepper, and Gaussian were applied to the images and the noisy images were filtered. The main reason of adding these noises to the DDH images was that USG images may have noises for other reasons including the probe, incorrect calibration of the device and environmental effects. In comparison to raw images, these noises added to the DDH images have lower qualities, which can cause an incorrect diagnosis. We have aimed to determine the negative effects of the noises in DDH images. Then, these images were segmented using the active contour model. In the last step, the PSNR and MSE values of the filtered images were evaluated. Figure 2 shows the block diagram of the steps involved in filtering the DDH images.

3.1. Image Quality Measurement

In their diagnosis of DDH, doctors often use the image captured of the right angle and detect the presence of DDH by looking at the femoral and acetabular regions. Therefore, to obtain the best accuracy, the area of the image showing these regions must be clearly displayed. In our work, PSNR and MSE distortion measurements are applied in order to compare the difference in the image quality between the original image and the output image.

Mean square error (MSE) is defined in the following way (6):

\[ \text{MSE} = \frac{1}{MN} \sum_{i=1}^{M} \sum_{j=1}^{N} (x(i,j) - \hat{x}(i,j))^2 \]  

where, \( x(i,j) \) is the original image, \( \hat{x}(i,j) \) is the output image, and \( MN \) represents the size of the image.

PSNR is defined in the following manner (6):

\[ \text{PSNR} = 20 \log_{10} \left( \frac{2^n - 1}{\sqrt{\text{MSE}}} \right) [dB] \]  

where, \( n \) is the number of bits per pixel used in the image. For a gray-level image, \( n = 8 \).

A higher PSNR value of the image indicates that it contains more valuable signals (6). In the same way, a low MSE value shows a lower rate of degradation in the image.
3.2. Image Segmentation Test

The basic idea of the active contour model is to develop curves converging towards the reference object, also known as the general curve fitting method (11-15). The curve to be segmented is selected around the object, and then, according to the effects of the internal and external forces, a converge operation is performed. When displaying the Figure of the resulting curves, the active contour model is divided into two types: open and closed (11, 14, 16-18).

The active contour without edges method is a closed type presented by Chan and Vese (CV) as a successful segmentation algorithm (11). The curve propagation of the algorithm is based on the Mumford-Shah method and level set technique (19). This method is less sensitive to noise than the other contour methods. As in the other contour models, this model also includes a function that minimizes energy levels.

When determining inner lines, the contour moves are not dependent on initial values. This feature distinguishes it from the Snake model. The zero level set of the displayed surface is an active curve, and this curve detects the object in the image. Due to the nature of this closed display, topological changes, such as segmentation and merging, can be detected automatically. In this method, an image is divided into homogeneous regions using this level function. These regions are composed of image parts comprised of closed field values (20).

The CV algorithm defines the $F(c_1, c_2, C)$ energy function for the $u_0$ image, which is divided into two parts with the C closed edge. The function is:

$$F(c_1, c_2, C) = \mu, length(C) + \nu, region(in(C))$$
$$+ \lambda_1 \int_{in(C)} |u_0(x, y) - c_1|^2 dx dy$$
$$+ \lambda_2 \int_{out(C)} |u_0(x, y) - c_2|^2 dx dy$$

where, $\mu \geq 0, \lambda_1, \lambda_2 > 0$ and are constant parameters, $c_1$ and $c_2$ are variables and $C$ are the mean values of the inner and outer regions, respectively. The first term is the regularization term that prevents a small area from merging with the latest detected contour due to noise.

The last two terms are the fitting terms. Using the analysis of the CV level set, the energy function equation is rewritten as (20):

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**Figure 2.** Image processing on developmental dysplasia of the hip (DDH) ultrasonography (USG) image used in this work.
The next stage of our study was to test the USG images. Based on the PSNR values shown in the tables, it was observed that the Wiener filter removes more noise than other filters for raw images, the median filter removes more noise than other filters for salt and pepper noise-added images, the Perona and Malik filter removes more noise than other filters for Gaussian noise-added images, and finally, the Lee filter removes more noise than other filters for speckle noise-added images.

The next stage of our study was to test the USG im-
Table 1. PSNR and MSE Values in the Raw Images

| Image          | Randomly Selected Image | Average Value of 10 Images |
|----------------|-------------------------|---------------------------|
|                | PSNR       | MSE       | PSNR       | MSE       |
| Frost          | 40.08      | 6.38      | 40.63      | 5.72      |
| Gaussian       | 38.56      | 9.07      | 39.05      | 8.20      |
| Lee            | 38.52      | 9.14      | 39.10      | 8.12      |
| Mean           | 38.22      | 9.80      | 38.71      | 8.86      |
| Median         | 40.31      | 6.06      | 40.92      | 5.37      |
| Perona Malik   | 30.57      | 56.99     | 31.12      | 50.67     |
| Wiener         | 42.83      | 3.39      | 43.49      | 2.97      |

Abbreviations: PSNR, peak signal to noise ratio; MSE, mean square error.

Table 2. PSNR and MSE Values in the Images with Gaussian Noise Added

| Image       | Randomly Selected Image | Average Value of 10 Images |
|-------------|-------------------------|---------------------------|
|             | PSNR       | MSE       | PSNR       | MSE       |
| Noisy       | 18.51      | 915.43    | 18.51      | 917.40    |
| Frost       | 23.62      | 282.41    | 23.58      | 285.21    |
| Gaussian    | 26.06      | 161.61    | 25.97      | 164.42    |
| Lee         | 26.02      | 162.67    | 25.96      | 164.82    |
| Mean        | 26.05      | 161.54    | 26.00      | 163.58    |
| Median      | 25.25      | 194.17    | 25.29      | 192.56    |
| Perona Malik| 27.71      | 100.12    | 27.68      | 111.81    |
| Wiener      | 24.35      | 238.98    | 24.31      | 241.27    |

Abbreviations: PSNR, peak signal to noise ratio; MSE, mean square error.

$^a\sigma^2 = 0.02.$

Table 3. PSNR and MSE Values in the Images Salt and Pepper Noise Added

| Image        | Randomly Selected Image | Average Value of 10 Images |
|--------------|-------------------------|---------------------------|
|              | PSNR       | MSE       | PSNR       | MSE       |
| Noisy        | 20.93      | 524.38    | 20.99      | 518.20    |
| Frost        | 26.69      | 139.23    | 26.58      | 142.91    |
| Gaussian     | 29.99      | 65.14     | 29.68      | 70.01     |
| Lee          | 29.83      | 67.56     | 29.66      | 70.33     |
| Mean         | 29.84      | 67.48     | 29.68      | 70.12     |
| Median       | 41.74      | 4.35      | 40.60      | 5.78      |
| Perona Malik | 22.98      | 327.29    | 22.93      | 332.24    |
| Wiener       | 21.74      | 435.97    | 21.74      | 435.83    |

Abbreviations: PSNR, peak signal to noise ratio; MSE, mean square error.

$^a\sigma^2 = 0.02.$

age segmentation method by applying the active contour method. This segmentation process is aimed to investigate the ilium. Firstly, all the images in the ilium were manually seg-
mented, and the center-point was determined. Then the center, right-end and left-end points was identified in the ilium region. Thus, the original image values were created. The process used for the automatic segmentation active contour method was tested in the filtered images (Figure 3). For the automatically segmented image in the ilium, center, right-end and left-end points were determined. To determine the success of the process of segmentation, the measures were compared (Table 5).

According to Table 5, Perona and Malik filtering had the best result (94.17993) as far as closeness to the raw image segmentation coordinate values. In addition, almost all filtering techniques applied in this study had close proximity values.

5. Discussion

In the literature, various methods of noise removal have been proposed and successfully implemented in USG images. The objective of the current study was to evaluate the efficiency of applying filters on USG images in order to increase the rate of DDH detection. Therefore, the study implemented seven different filters and evaluated their efficiency when applied to USG images of pure and noise-added DDH images. A variety of filter configurations was simulated to remove noise, and the results for different filters were obtained. Based on proximity values shown in Table 5, it is observed that filters applied to the DDH images on the segmentation process have low influence. However, in some cases this effect, which appears small, may lead to serious consequences. However, the study concluded that two or three filters should be used together, and that the segmentation method should be used to measure the image quality.

Previous studies have targeted enhancing USG image quality by applying different filters. The success rate of enhancement depends on the probe of the device, the acquisition angle, the noise type in the image, filter parameters and assessment criteria. Therefore, it is not appropriate to compare our study with other studies (22-26).

In our study, it was observed that the Wiener filter removed more noise than other filters for raw images, with the highest average PSNR value (43.49), the median filter removed more noise than other filters for salt and pepper noise-added images, with the highest average PSNR value (27.68), the Perona and Malik filter removed more noise than other filters for Gaussian noise-added images, with the highest average PSNR value (40.60) and finally, the Lee filter removed more noise than other filters for Speckle noise-added images, with the highest average PSNR value (35.35).

When we analyzed the literature regarding segmentation of hip joints, it was seen that all results were reported as promising, but numerical results were not shown. In our study, active contour model-based segmentation was implemented for obtaining the femur region and compared with a manually segmented femur region. As a result of this process, Perona and Malik filtered images segmented properly (7-10).

However, there are limitations as well. From a diagnostic point of view, only the ilium region segmentation was not adequate. After acetabulum region segmentation, angular values (α, β) should be determined in real time. These values should be compared to a radiologist’s values. All of these processes must be implemented for computer-aided diagnosis of DDH in real time.

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Table 4. PSNR and MSE Values in the Images Speckle Noise Added

| Image         | Randomly Selected Image | Average Value of 10 Images |
|---------------|-------------------------|---------------------------|
|               | PSNR       | MSE       | PSNR       | MSE       |
| Noisy         | 28.62      | 89.39     | 28.36      | 96.71     |
| Frost         | 33.38      | 29.89     | 33.37      | 30.71     |
| Gaussian      | 34.97      | 20.70     | 35.30      | 19.37     |
| Lee           | 34.88      | 21.15     | 35.35      | 19.14     |
| Mean          | 34.74      | 21.82     | 35.20      | 19.81     |
| Median        | 32.83      | 33.86     | 32.94      | 33.41     |
| Perona Malik  | 30.30      | 60.63     | 31.26      | 49.11     |
| Wiener        | 31.75      | 43.45     | 31.63      | 45.12     |

Abbreviations: PSNR, peak signal to noise ratio; MSE, mean square error.

*$σ^2 = 0.05.$
Table 5. Image Segmentation Test Results

| Position | Original | Noisey | Front | Gaussian | Lee | Mean | Median | Perona-Malik | Wiener |
|----------|----------|--------|-------|----------|-----|------|--------|--------------|--------|
| C        | 100      | 96.10803 | 96.10656 | 96.12633 | 96.09667 | 96.09667 | 96.13771 | 95.26996 | 96.1050 |
| R-E      | 100      | 96      | 96     | 96     | 96     | 96     | 96     | 96.39445 | 96.3951 |
| L-E      | 100      | 96.83772 | 96.83772 | 96.83772 | 96.83772 | 96.83772 | 96.83772 | 96.83772 | 96.83772 |
| C        | 100      | 97.0778 | 97.0778 | 97.0778 | 97.0778 | 97.0778 | 97.0778 | 97.0778 | 97.0778 |
| R-E      | 100      | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 |
| L-E      | 100      | 96      | 96     | 96     | 96     | 96     | 96     | 96     | 96     |
| C        | 100      | 98.00608 | 88.47341 | 88.91421 | 88.62444 | 88.60048 | 88.50559 | 88.50559 | 88.50559 |
| R-E      | 100      | 87.97044 | 87.97044 | 87.97044 | 87.97044 | 87.97044 | 87.97044 | 87.97044 | 87.97044 |
| L-E      | 100      | 98      | 98     | 98     | 98     | 98     | 98     | 98     | 98     |
| C        | 100      | 88.85360 | 89.85360 | 89.85360 | 89.85360 | 89.85360 | 89.85360 | 89.85360 | 89.85360 |
| R-E      | 100      | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 | 97.1517 |
| L-E      | 100      | 98.00608 | 88.47341 | 88.91421 | 88.62444 | 88.60048 | 88.50559 | 88.50559 | 88.50559 |
| C        | 100      | 96.88377 | 96.88377 | 96.88377 | 96.88377 | 96.88377 | 96.88377 | 96.88377 | 96.88377 |
| R-E      | 100      | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 |
| L-E      | 100      | 98      | 98     | 98     | 98     | 98     | 98     | 98     | 98     |
| C        | 100      | 89.95012 | 89.95012 | 89.95012 | 89.95012 | 89.95012 | 89.95012 | 89.95012 | 89.95012 |
| R-E      | 100      | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 | 95.87689 |
| L-E      | 100      | 98      | 98     | 98     | 98     | 98     | 98     | 98     | 98     |
| C        | 100      | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 |
| R-E      | 100      | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 |
| L-E      | 100      | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 | 92.59265 |
| Average  | 100      | 94.12537 | 94.06054 | 94.01740 | 94.01016 | 94.02689 | 94.02871 | 94.17993 | 94.08641 |

Abbreviations: C, Center; R-E, Right-End; L-E, Left-End.
Figure 3. DDH image. A, Manually segmented image; B, Manually segmented image binary for C,R-E,L-E points; C, Raw image; D, Automatically segmented image binary for C,R-E,L-E points (C, Center; R-E, Right-End; L-E, Left-End).

Acknowledgments

This study was carried out in Selcuk university, department of computer engineering as a doctoral thesis.

Footnotes

Authors’ Contribution: The study was carried out as a part of a doctoral thesis. Hasan Erdinc Kocer, the author of the paper, is the PhD supervisor. Kerim Kursat Cevik, the second author of paper, is the PhD student. Mesut Sivri and Mustafa Koplay, the third and fourth authors of paper, provided USG. They work as experts to determine the ilium and femur points.

Financial Disclosure: There has been no fund as a support for the study. In addition, the authors of this study do not expect any financial interests.

Funding/Support: DDH Images were obtained from Selcuk university, faculty of medicine, radiology department.

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