DYNAMICS AND CONTROL OF THE GYROSCOPIC HEAD USED FOR THE LASER ILLUMINATION OF A GROUND TARGET FROM THE QUADCOPTER DECK

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Resume
In the paper authors investigate dynamics of a controlled quadcopter in terms of the possibility of its use for detection, observation, tracking and laser illuminating of both stationary and moving ground targets in the conditions of impact of random and kinematic excitations. The drone is equipped with a scanning and tracking Gyroscopic Head (GH) coupled with a laser target indicator. The drone is affected by random disturbances in the form of wind gusts or explosions of missiles. Kinematic excitations, such as drone maneuvers and vibrations from engines, act on the GH. This paper focuses mainly on control and stabilization of the gyroscopic head placed on the drone during the search, tracking and simultaneous laser illuminating of the target.

1 Introduction
In recent years, four-rotor unmanned aerial vehicles (quadcopters) have become a very popular unmanned platform that is still in the stage of intensive research and finds a variety of applications. Currently, they are used, among others, for shooting collective events, monitoring communication infrastructure, supporting rescue operations, monitoring the state of air pollution. The paper proposes the use of this type of QuadCopter Unmanned Aerial Vehicle (QCUAV) for the laser pointing of ground targets, both stationary and mobile, using the scanning and tracking gyroscopic head [1-2]. In addition, a mathematical model was developed for controlling the movement of the gyroscopic scanning and tracking head as well as the mathematical model of the drone’s dynamics [3-5].

It should be emphasized that the advantage of the considered QCUAV is its ability to stay in hover for a certain period of time. The system of laser pointing of a target (SLPT) can thus act independent from drone’s movement and therefore stably determines the target observation line (T-LOS) regardless of disturbances acting on the drone itself. While searching for a target, the GH is put into a programmed motion that allows scanning the ground surface [6]. The infrared sensor and the laser target pointer are attached to the GH axis. At the moment of receiving a thermal signal from the target, the drone goes to hover and GH begins to illuminate it with laser pulses, so that target can become the object of attack [7-8].

To ensure the high precision in maintaining the T-LOS in a given position, an optimal controller was designed for the GH. For this reason, despite many control methods used for the unmanned aerial vehicle, known in the literature [9-11] a simple PID controller was used to control the flight of the QCUAV, since the drone movement in space does not have to be precisely determined [12-16]. Simplified operation diagram of the system of detection, tracking and laser pointing of a target from the QCUAV deck is shown in Figure 1.

2 Mathematical model of dynamics of the QCUAV and controlled gyroscopic head

The executive unit in the scanning and tracking head, mentioned above, is a controlled gyroscope system. The general view of the gyroscope system with forces and moments of forces is shown in Figure 2.

Mathematical model of the controlled gyroscope system dynamics is presented in the following form [17]:

\[
J_z \frac{d\omega_{r1}}{dt} + (J_z + J_x) \frac{d}{dt}(\omega_{r1}\cos\theta_x) - J_x \times \\
\times \frac{d}{dt}(\omega_{r1}\sin\theta_x) - J_x \frac{d}{dt}(\omega_{r2}\sin\theta_x) + m \frac{d}{dt} \times \\
\times \frac{d}{dt}(V_{r2}(1 + \cos\theta_x)) + (J_z + J_x)\omega_{r1}\omega_{r2} + \\
+ (J_x + J_z)\omega_{r2}\omega_{r1} - (J_x + J_z)\omega_{r2}\omega_{r1}\sin\theta_x -
\]

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Figure 1 Simplified operation diagram of the system of detection, tracking and laser pointing of a target from the QCUAV deck.

Figure 2 General view of the gyroscope system.
\[-(J_3\omega_{z3} + J_3\omega_{z3})\omega_{z3}\cos\theta_z - m_xV_{x3}[V_{x3}\cos\theta_z - \omega_{z3}l_x\sin\theta_z] = = U_x - U_{z3},\]

\[(J_{z1} + J_{z2})\frac{d\omega_{z1}}{dt} - m_yl_y\frac{dV_{z3}}{dt} - (J_{z1} + J_{z2})\times\times\omega_{z3}\omega_{x3} - J_{z2}\omega_{z3}\omega_{x3} - m_yl_yV_{x3}\omega_{z3} - m_yV_{x3}\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\times\time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with
\[ \dot{\omega} = \Omega_1 + \Omega_2 - \Omega_3 - \Omega_4; \]
\[ \Omega_1, \Omega_2, \Omega_3, \Omega_4; \] - rotational speeds of the individual motors,
\( l_i \) - arm's length,
\( m_i \) - drone's mass,
\( I_{x}, I_{y}, I_{z} \) - moments of inertia of the QCUAV,
\( J_r \) - moment of inertia of the rotor and
\( U_{1}, U_{2}, U_{3}, U_{4} \) - controls.

The control vector \( \mathbf{U} \) is determined by the following formula:
\[
\begin{bmatrix}
U_1 \\
U_2 \\
U_3 \\
U_4
\end{bmatrix} =
\begin{bmatrix}
-b(\Omega_1^2 + \Omega_2^2 + \Omega_3^2 + \Omega_4^2) \\
b(\Omega_1^2 - \Omega_2^2) \\
b(\Omega_2^2 - \Omega_3^2) \\
d(\Omega_1^2 + \Omega_3^2 - \Omega_2^2 - \Omega_4^2)
\end{bmatrix}
\]

where \( b \) is the thrust coefficient and \( d \) is the drag coefficient.

3 Results and conclusions

In order to verify the correct operation of the gyro head during the laser illuminating the ground target from the deck of drone, appropriate simulation tests were carried out. The drone movement from a given starting point in space to a point on a fixed height \( H_d = 20 \text{ m} \) - exactly above and at a fixed distance from the target, moving on the surface of the earth, was considered. The drone's GH tracks the moving target and at the same time illuminates it with a laser. This is shown in the Figures 4-12.

The tests were conducted in the Matlab/Simulink environment using the ode45 integration procedure for the following parameters:

- gyro system parameters
  \( J_{11} = 2.5 \times 10^{-7} \text{ kgm}^2; J_{12} = J_{13} = J_{23}; \)
  \( J_{x} = 5 \times 10^{-5} \text{ kgm}^2; J_{x1} = J_{x3} = J_{23}; \)
  \( J_{x2} = 2.5 \times 10^{-4} \text{ kgm}^2; J_{x3} = J_{x1} = 5 \times 10^{-4} \text{ kgm}^2; \)
  \( n_s = 600 \text{ rad/s}; \eta_k = 0.01 \text{ Nms}; \eta_e = 0.01 \text{ Nms}; \)
  \( m_p = 0.24 \text{ kg}; l_0 = 0.001 \text{ m}; \)
- optimal LQR gain matrix for the gyro system
  \[ \mathbf{K}_p = \begin{bmatrix}
9.5114 & 0.3709 & 41.9258 & 0.1695 \\
-2.0134 & 0.0004 & 0.4585 & 0.0031
\end{bmatrix} \]
- quadcopter parameters
  \( m_s = 0.65 \text{ kg}; l_s = 0.23 \text{ m}; b = 3.13 \times 10^{-5} \text{ Nms}^2; \)
  \( d = 7.5 \times 10^{-7} \text{ Nms}^2; \eta_s = 6.0 \times 10^{-5} \text{ kgm}^2; \)
  \( \Omega_{max} = 500 \text{ rad/s}; I_s = 7.5 \times 10^{-3} \text{ kgm}^2; \)
  \( I_s = 7.5 \times 10^{-3} \text{ kgm}^2; L = 1.3 \times 10^{-2} \text{ kgm}^2; \)

the values of the PID regulator coefficients for the drone
\( k_{p1} = 11.8; k_{d1} = 10.8; k_{i1} = 0.9; \)
\( k_{p2} = 0.65; k_{d2} = 0.46; \)
\( k_{p3} = 0.45; k_{d3} = 0.36; \)
\( k_{p4} = 0.12; k_{d4} = 0.12; \)
\( k_{p5} = 8.8; k_{d5} = 8.9; \)
\( k_{p6} = 8.8; k_{d6} = 8.9. \)

The graphs show the movement of the gyroscope axis, having the task at keeping the line of sight from
visible, after which the compensator follows the target with sufficient accuracy. However, it should be noted, that the transitional period also appears when the drone is moved to hover and lasts only about 0.5 s. It was also assumed that during the reaching heights and hover, the wind is blowing on the drone. These gusts significantly disturb the drone flight trajectory, however, they do not have much

the deck of the drone from the moment of gaining the height to the passage and maintaining the hover. At the starting moment of the drone, the initial conditions of the gyroscope axis motion are unknown. For this reason, a series compensator was used (the state observer with the LQR controller). In the initial phase of tracking, i.e. for a period of about 1 second, the large dynamic effects are
impact on accuracy of the target illumination by the gyro axis. In figures, the position of the gyro axis determines the angles $\theta_{\text{tag}}$ and $\psi_{\text{sig}}$ (blue), while the set position is $\theta_{\text{tag}z}$ and $\psi_{\text{sig}z}$ angles (yellow) and angles determined by the observer are $\theta_{\text{tag}obs}$ and $\psi_{\text{sig}obs}$.

Initial simulations demonstrated that the system laser illuminating ground target from the deck of a drone, using the gyro scanning and tracking head, is robust to large external interference from QCUAV and even its complete descent from both the pre-set trajectory and the hovering.

In addition, the gyro head and drone control algorithm proposed in this paper works correctly and ensures the precise laser target illumination capability.
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