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Cataract surgery patient-reported outcome measures: a head-to-head comparison of the psychometric performance and patient acceptability of the Cat-PROM5 and Catquest-9SF self-report questionnaires

Abstract

Background Cataract surgery is the most frequently undertaken NHS surgical procedure. Visual acuity (VA) provides a poor indication of visual difficulty in a complex visual world. In the absence of a suitable outcome metric, recent efforts have been directed towards the development of a cataract patient-reported outcome measure (PROM) of sufficient brevity, precision, and responsiveness to be implementable in routine high volume clinical services.

Aim To compare and contrast the two most promising candidate PROMs for routine cataract surgery.

Method The psychometric performance and patient acceptability of the recently UK developed five-item Cat-PROM5 questionnaire was compared with the English translation of the Swedish nine-item Catquest-9SF using Rasch-based performance metrics and qualitative semistructured interviews.

Results Rasch-based performance was assessed in 822 typical NHS cataract surgery patients across four centres in England. Both questionnaires demonstrated good to excellent performance for all metrics assessed, including Person Reliability Indices of 0.90 (Cat-PROM5) and 0.88 (Catquest-9SF), responsiveness to surgery (Cohens standardized effect size) of 1.45 SD (Cat-PROM5) and 1.47 SD (Catquest-9SF) and they were highly correlated with each other ($R = 0.85$). Qualitative assessments confirmed that both questionnaires were acceptable to patients, including in the presence of ocular comorbidities. Preferences were expressed for the shorter Cat-PROM5, which allowed patients to map their own issues to the questions as opposed to the more restrictive specific scenarios of Catquest-9SF.

Conclusion The recently UK developed Cat-PROM5 cataract surgery questionnaire is shorter, with performance and patient acceptability at least as good or better than the previous ‘best of class’ Catquest-9SF instrument.

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Introduction

Cataract is a common potentially blinding eye disease with an adverse impact on quality of life for which surgical intervention is currently the only effective treatment. In England during the year 2015–2016 there were over 390 000 cataract operations undertaken in the UK National Health Service (NHS), representing a crude rate of ~ 7.0 per 1000 population, with in addition over 13 000 postcataract posterior capsulotomies at a combined estimated cost of ~ £400 million.
In the face of high demand, shrinking NHS resources and variations in eye care, taking account of the overall impact of cataract on a patient’s life is of increasing importance. The 2017 National Institute for Health and Care Excellence (NICE) cataract surgery guideline (NG77) and the Royal College of Ophthalmologists 2015 cataract surgery commissioning guideline both recommend further research into self-reported measures of visual disability caused by cataract, including patient-reported outcome measures (PROMs) for cataract surgery. In addition to the usual requirements of validity and robust psychometric performance, a NHS-suitable cataract surgery PROM would need to be brief to be implementable in high volume service environments. Among the various measures two instruments appear to be the most promising candidates: the English translation of the Swedish Catquest-9SF, and the more recently UK developed Cat-PROM5. Each are short, psychometrically robust instruments validated in English-speaking contexts. In this report we compare and contrast their psychometric properties. Determination of the final item set was inﬂuenced by statistical considerations, a patient ‘co-researcher’ advisory group and expert view. As part of the Cat-PROM5 development work, completions of the Catquest-9SF questionnaire were simultaneously obtained from participants, allowing a direct comparison of the performance of both instruments.

Methods

Participants

Analyses presented here are based on a group of 822 patients recruited from four cataract surgical centres in England (Bristol, Torbay, Cheltenham, Brighton). Data for the study were collected in three separate cycles (Pilot, Cycle 1, and Cycle 2). To estimate sensitivity to surgical intervention (effect size), participants in Cycles 1 and 2 were asked to complete questionnaires both before and after their cataract operation.

Analytical strategy

Comparative analysis was conducted by means of separate Rasch calibrations of both questionnaire instruments. In both analyses, we used the Partial Credit Model available within the Winsteps analysis program (www.winsteps.com).

Because the study included repeated measurements (before and after surgery) for Cycles 1 and 2, there was an issue with violation of the Rasch analysis assumption of independence of observations. The Rasch analyses were therefore split into two phases, calibration and scaling. In the first (calibration) phase, participants who had contributed two questionnaire completions had either their pre- or postoperative completion (never both) randomly...
selected for inclusion in the analysis set, a procedure that avoided violation of the independence assumption. This set of data was Rasch analysed and the item parameters (difficulties and Rasch–Andrich thresholds) established. These were then used at the next stage as anchors for estimation of the person parameters for the participant’s alternative (pre- or postoperative) completion. This analytical schedule avoided the problem of case dependency within the data, yet provided person estimates for two time points, thus allowing valid comparisons of the outcomes of pre- and postoperative groups.

Having completed analyses separately for Cat-PROM5 and Catquest-9SF, the performance of both scales was compared with regard to three general questions: (1) Do they both measure the same construct? (2) How precise are each of the scales? (3) How well does each function when applied to typical UK NHS cataract patients? The first was assessed in terms of the correlation between the two questionnaires, we assumed a correlation of 0.70 (nearly 50% of common variance) or above would be sufficient. Precision of each was assessed using two reliability indexes: Rasch-based reliability (the share of the ‘true’ variance in the total observed variance of the measure) and the classical Cronbach’s $\alpha$ with 0.70 to $<0.80$ regarded as acceptable, 0.80 to $<0.90$ as good, and 0.90 or above as excellent. To answer the final question, we compared performance of both scales on several criteria providing insights on the functioning of each in a UK context. Since Catquest-9SF was developed and validated in other cultural and geographical contexts (Sweden and Australia), it was deemed important to assess these elements on a relevant UK patient group. We assessed these criteria: Rasch–Andrich item thresholds ordered in the expected (increasing) order; item fit (mean square out/infinit statistics within 0.7–1.3); point-measure item correlation ($\geq0.4$); category averages increasing monotonically along the Rasch continuum; unidimensionality (highest eigenvalue of residual correlation matrix $<2.0$); item invariance (Differential Item Functioning or DIF, assessed by both significance testing and by differential magnitude following the Educational Testing Service classification of DIF): $>0.63$ as being large); responsiveness to surgery adopting Cohen’s classification of standardized effect sizes (ES: $>0.50$ moderate; $>0.80$ large, i.e., the higher the ES the more responsive is the scale to surgical intervention); and completion burden (number of items).

A qualitative study on a separate group of patients explored the face-validity and acceptability of each questionnaire (in terms of language, accuracy, and relevance), particularly for those with visual comorbidities. A purposeful sampling strategy was used to include perspectives from a range of visual comorbidities. Participants included men and women of varying ages as well as pre- or postoperative status. Semistructured face-to-face interviews were guided by a topic guide to ensure that discussions covered the same basic issues, but with sufficient flexibility to allow emergence of new issues of importance, and with new points added as analysis progressed to enable exploration of emerging themes and encourage more detailed responses. Where uncertainties arose, respondents were asked how they understood the items and encouraged to explain their reasoning and reflect on their overall perceptions of the questionnaire. Data were analysed using techniques of constant comparison derived from grounded theory methodology, and emerging themes and codes within transcripts and across the dataset were then compared to look for shared or disparate views among participants. Data collection and analysis continued until the point of data saturation.

Results

Sociodemographic characteristics for participants have previously been reported. Briefly, participants mean age was 76 years, 58% were female and 67% were undergoing surgery in their first eye. The respondents’ results (Rasch measure) on both scales showed a strongly positive association with a linear correlation of $R = 0.85$ ($P < 0.001$; $N = 1189$ completions). Figure 1 presents a Bland–Altman plot of agreement incorporating the distribution of the means along the horizontal axis and the distribution of the differences along the vertical axis. Table 1 provides details of the performance of both questionnaires, and Table 2 summarizes comparative performance based on the parameters noted above.

From both tables it is apparent that each scale performs well with only moderate to small relative differences.

![Figure 1](image-url)
Table 1  Quality of the measurement models of Cat-PROM5 and Catquest-9SF across all cycles combined

| Item          | Rasch measure—item difficulty (SE) | Infit MnSQ | Outfit MnSQ | Point-measure correlation | Rasch–Andrich thresholds (centralized to item difficulty) |
|---------------|------------------------------------|------------|-------------|---------------------------|----------------------------------------------------------|
| Cat-PROM5     |                                    |            |             |                           |                                                          |
| VSQ_Bad_Eye   | −0.89 (0.09)                       | 1.12       | 1.11        | 0.80                      | −3.11 0.46 2.65 — — —                                   |
| Interere      | −0.06 (0.08)                       | 0.73       | 0.76        | 0.89                      | −4.17 −2.29 −0.16 2.39 4.23 —                           |
| VSQ_Overall   | −0.51 (0.08)                       | 1.02       | 1.01        | 0.88                      | −7.70 −3.02 −0.84 1.14 3.88 6.55                       |
| VSQ_Doing     | 1.41 (0.11)                        | 0.91       | 0.87        | 0.77                      | −3.56 0.72 2.85 — — —                                   |
| VSQ_Reading   | 0.05 (0.08)                        | 1.18       | 1.14        | 0.82                      | −3.53 −1.70 1.09 4.14 — — —                             |
| Catquest-9SF  |                                    |            |             |                           |                                                          |
| Cat_Vision    | 0.26 (0.09)                        | 0.92       | 0.83        | 0.78                      | −3.98 1.60 2.38                                       |
| Cat_Satisfied | −1.80 (0.08)                       | 1.32       | 1.32        | 0.78                      | −3.22 0.24 2.98                                       |
| Cat_Read      | −0.39 (0.08)                       | 0.96       | 0.97        | 0.79                      | −3.08 1.38 1.70                                       |
| Cat_Faces     | 1.80 (0.09)                        | 1.19       | 1.10        | 0.62                      | −2.08 0.36 1.71                                       |
| Cat_Prices    | −0.16 (0.07)                       | 0.93       | 0.98        | 0.79                      | −2.82 0.94 1.88                                       |
| Cat_Ground    | 0.70 (0.08)                        | 1.10       | 1.25        | 0.71                      | −2.49 0.50 1.99                                       |
| Cat_Handwork  | −0.16 (0.07)                       | 0.80       | 0.76        | 0.81                      | −2.43 0.75 1.68                                       |
| Cat_Text_TV   | −0.28 (0.07)                       | 0.98       | 1.03        | 0.79                      | −2.64 0.76 1.88                                       |
| Cat_Activity  | 0.03 (0.07)                        | 0.75       | 0.66        | 0.81                      | −2.42 0.73 1.69                                       |

Table 2  Summary of quality of both measures

Which measures were more difficult for participants? The Rasch measure—item difficulty is presented in Table 1.

| Statistics            | Cat-PROM5 | Catquest-9SF |
|-----------------------|-----------|--------------|
| Person reliability index | 0.90     | 0.88         |
| Cronbach’s α          | 0.89      | 0.92         |
| Variance explained     | 72%       | 64%          |
| Variance explained by patients | 55%  | 48%         |
| Variance explained by items | 16%     | 16%          |
| Variance unexplained   | 28%       | 36%          |
| Highest residual eigenvalue | 1.5 | 1.6         |
| Number of items        | 5         | 9            |
| Number of misfitting items (Infit/Outfit out of range 0.7–1.3) | 0 | 2 |
| Number of reversed thresholds | 0 | 0 |
| Number of reversed category means | 0 | 0 |
| Number of statistically significant DIF instances | 3 (7.5%) | 3 (4.2%) |
| Number of instances of ‘large’ DIF, i.e. | 1 (2.5%) | 2 (2.8%) |
| Cohens’s standardized effect size | −1.45 | −1.47 |
| Cohens’s standardized effect size | −1.09 | −1.14 |

*Educational Testing Service criteria http://www.ets.org/Media/Research/pdf/RR-12-08.pdf). *Denominator as SD from preop time point. *Denominator as SD for the whole sample (including both pre- and postoperatively).

Figure 2 provides ‘Person-Item’ or ‘Wright’s maps’ for both scales illustrating the positions for each item and each of their levels. Preoperatively there were no ceiling or floor effects for either scale. Postoperatively there was a moderate floor effect for Cat-PROM5, with 9% of respondents reporting no problems and for Catquest-9SF a more obvious floor effect, with 25% reporting no problems. Figure 3 depicts the DIF plots for each scale for assessment of item invariance across eight groupings of participants (e.g. older vs younger), showing that with very few exceptions the performance of the individual items is invariant across these groupings.

In the qualitative study 16 interviews were conducted with nine men and seven women with a mean age of 75 years (range 57–92). Eleven patients were awaiting their cataract surgery, and five had recently undergone surgery. Thirteen participants had other visual comorbidities, including age-related macular degeneration (wet and dry), myopic macular degeneration, amblyopia, glaucoma, retinal vascular occlusion, previous retinal detachment, Fuchs endothelial dystrophy, and neurological visual field loss. Interviews lasted an average of 50 min (range = 24–73). Overall both questionnaires were well received, although patients with severe visual comorbidities commented that it was difficult to differentiate between how the cataract and other conditions affected their quality of life. Most participants preferred the large-font format of Cat-PROM5. Some preferred questions with more response options as in Cat-PROM5, and others fewer response options as in Catquest-9SF. The specific scenarios of Catquest-9SF created some uncertainty where other health problems affected the issue being addressed, and where the issue was not relevant to their lives respondents were uncertain about how to respond. In contrast, Cat-PROM5 enabled them to determine the individual vision-related factors which they perceived to be important, and to respond to the questions easily.
**Discussion**

The strong linear correlation ($R = 0.85$) between the scales provides empirical evidence that both scales are measuring the same theoretical concept. The Bland Altman plot with distributions illustrates good agreement between individual person measures derived separately from the two questionnaires. Each has a similar high level of precision; Cat-PROM5 achieves ‘excellent’ reliability based on the

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**Figure 2** Person-Item or Wright’s maps illustrating the distributions of patient responses in the upper panel from those with two cataracts, in the second panel from those with one cataract (a cataract in one eye and either pseudophakia or a clear crystalline lenses in the other), and in the third panel those with no cataracts (either bilateral pseudophakia or pseudophakia in one eye and a clear crystalline lenses in the other). The lower panel in (a) shows the positions of the Item Locations (Loc) and Category Thresholds (T#) for Cat-PROM5 and (b) shows these similarly for Catquest-9SF. All panels refer to the same horizontal scale from $-9$ to $+9$ logits.
Rasch model, while Catquest-9SF achieves this level on the classical Cronbach’s $\alpha$. It should be noted, however, that this latter coefficient is in part dependent on the number of questions included in the scale and Catquest-9SF has almost twice as many questions as Cat-PROM5. In the context of a scale intended for use in high volume cataract surgical services, a longer scale has potential logistical and cost disadvantages that need to be borne in mind. From these results, however, it is clear that both scales display high precision with the shorter Cat-PROM5, perhaps having an edge over the longer Catquest-9SF. Both scales fit the data well with fitting indices mostly within acceptable limits, no reversed thresholds, and point-measure correlations positive and reasonably high. Both scales are unidimensional constructs with the highest eigenvalues in each case below 2.0 (Cat-PROM5 1.5, Catquest-9SF 1.6). Had an alternative
more stringent criterion of a highest eigenvalue threshold of 1.5 or less been used, unidimensionality would however have been borderline.

Person-Item or Wright’s maps for both scales (Figure 2) illustrate good span and targeting, with both scales performing similarly with a slightly wider (better) range observed for Cat-PROM5. There were no ceiling effects for either scale, although a notable postoperative floor effect (25%) was evident for Catquest-9SF. It should be borne in mind that following successful cataract surgery in both eyes vision would be expected to have been restored to normal or near normal in the absence of visually significant comorbidities. Cat-PROM5 would, however, be more sensitive to detection of relatively minor postoperative residual visual difficulties. Both scales were highly responsive to surgical intervention, the estimated effect sizes or Cohen’s delta for each being very large, marginally greater for Catquest-9SF. Based on the theoretically more relevant preop SD calculation, these were both near −1.5 SD and based on the alternative pooled sample SD near −1.1SD (both calculation methods have been provided here for purposes of comparison with other published results). It is worth noting that an effect size (group difference) of >0.8SD is regarded as a ‘large’ effect.

Item performance was mostly invariant for both measures across a range of groupings. In Table 2 and Figure 3 the number of statistically significant violations of invariance measured by DIF was 3 for both Catquest-9SF and Cat-PROM5. Of these, 2 were deemed ‘large’ for Catquest-9SF and 1 for Cat-PROM5. A statistically significant and large DIF thus occurred in less than 5% of all comparisons for each instrument.

The qualitative study indicated that both questionnaires were well received. Participants varied in regard to ease of completion of fewer (Catquest-9SF) or more (Cat-PROM5) item response options. On the whole, patients preferred that the Cat-PROM5 questionnaire enabled them to determine the individual vision-related factors which they perceived to be important, and to respond to the questions accordingly. In contrast the specific scenarios of Catquest-9SF provided particular instances that were sometimes not relevant to patients’ lives, and there was little opportunity to capture the ways in which cataract did affect their lives beyond those specific scenarios. The questions in Cat-PROM5 have previously been shown to have high face-validity for the majority of cataract patients, affirmed by the qualitative element of this work.

Conclusion

In this report Cat-PROM5 was compared against the English translation of Catquest-9SF, a widely used originally Swedish cataract PROM instrument. These results show that both scales measure the same concept with high precision, are unidimensional, conform to the stringent Item Response Theory requirements of the Rasch model, and are highly responsive to cataract surgical intervention with very large effect sizes of around 1.5SD (baseline SD). The less restrictive Cat-PROM5 questions were preferred by patients, and at almost half the length this would seem the more feasible implementation option for measurement of visual difficulty related to cataract and its relief from surgery in high volume surgical services such as those of the UK NHS.

Summary

What was known before
- The ‘patient’s view’ is increasingly recognized as a key measure in health service delivery.
- Patient’s self-reported visual difficulty related to cataract can be reliably measured using questionnaire instruments which must be brief to be implementable in high volume services.
- Cat-PROM5 and Catquest-9SF both demonstrate good psychometric performance with high responsiveness to surgery.

What this study adds
- A head-to-head comparison between the best two candidate instruments demonstrates that both perform equally well psychometrically.
- Patients preferred Cat-PROM5 in terms of it being almost half the length of Catquest-9SF and less proscriptive, allowing them to map their own visual difficulties to the questions.

Conflict of interest

The authors declare no conflict of interest.

Author contributions

JMS, overall responsibility for the study as chief investigator, conception and design of the study, obtaining funding for the study, writing, and approving manuscript; MTG, statistical analyses and writing manuscript; NAF, overseeing study as local principal investigator, interpretation of data, and reviewing and approving manuscript; RLJ, overseeing study as local principal investigator, interpretation of data, and reviewing and approving draft manuscript; CSCL, overseeing study as local principal investigator and approving manuscript; LE, managing the study, overseeing acquisition of data, and reviewing and approving manuscript; AL, managing the study, overseeing acquisition of data, collection of data, and reviewing and approving manuscript; DE, design, data collection and analysis of qualitative study elements, and reviewing and approving of manuscript; JLD, design
overall and of qualitative study elements, obtaining funding for the study, and reviewing and approving of manuscript.

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