Ultra-long-wavelength Dirac plasmons in graphene capacitors

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Abstract

Graphene is a valuable 2D platform for plasmonics as illustrated in recent THz and mid-infrared optics experiments. These high-energy plasmons however, couple to the dielectric surface modes giving rise to hybrid plasmon-polariton excitations. Ultra-long wavelengths address the low energy end of the plasmon spectrum, in the GHz–THz electronic domain, where intrinsic graphene Dirac plasmons are essentially decoupled from their environment. However experiments are elusive due to the damping by ohmic losses at low frequencies. We demonstrate here a plasma resonance capacitor (PRC) using hexagonal boron-nitride (hBN) encapsulated graphene at cryogenic temperatures in the near-ballistic regime. We report on a 100 μm quarter-wave plasmon mode, at 40 GHz, with a quality factor Q ≈ 2. The accuracy of the resonant technique yields a precise determination of the electronic compressibility and kinetic inductance, allowing to assess residual deviations from intrinsic Dirac plasmonics. Our GHz frequency capacitor experiment constitutes a first step towards the demonstration of plasma resonance transistors for microwave detection in the sub-THz domain for wireless communication and sensing. It also paves the way to the realization of doping-modulated superlattices where plasmon propagation is controlled by Klein tunneling.
plasmons propagate along a hBN-graphene-hBN-metal strip line of length $L \approx 24 \, \mu\text{m}$ and aspect ratio $L/W = 3$ (figure 1(c)). We report on the fundamental mode, which is a quarter-wave resonance at $f_0 = v_p/4L \sim 40$ GHz, where we achieve a quality factor $Q \approx 2$ at low temperatures ($T = 10$ K) corresponding to a damping length $\alpha^{-1} = 2QL/\pi \sim 30 \, \mu\text{m}$.

Our graphene resonator is a T-shape hBN-encapsulated single-layer graphene sample covered by a top metallization serving both as radio-frequency (RF) port and DC gate (see methods, figures 1(c) and 3). We have measured a series of eight devices, using both exfoliated and CVD graphene, but the results presented below focus on sample PRC6 ($L \times W = 24 \times 8 \, \mu\text{m}$) which has the highest mobility and largest quality factors. The device is embedded in a coplanar waveguide (CPW) and its RF gate-source admittance $Y(f, n, T)$ is measured in the range $f = 0\sim40$ GHz, $n = 0 \sim 2 \times 10^{12} \, \text{cm}^{-2}$ and $T = 10 \sim 300$ K using standard vector-network-analyzer (VNA) techniques (see methods and [15]). The strip line access, which has a broader width, constitutes the device source. It is equipped with a low-resistance edge contact (figure 1(c)). The source end of the strip is an impedance short, securing a plasmon node, the open end of the strip being an antinode so that the PRC sustains odd harmonics of the fundamental mode $f_0 = v_p/4L$.

We describe propagation by a distributed-line model (figure 1(b)). The line capacitance $C$ is the series addition of the insulator capacitance $C_{\text{ins}} = \epsilon W/d$ and the quantum capacitance $C_Q = \frac{e^2}{\hbar} \frac{kW}{v_F}$ (low temperature). The large top-gate capacitance enhances the $C_Q$ contribution and gives access to a capacitance spectroscopy which is used below to determine the Dirac-point position. The line inductance is dominated by the kinetic contribution, which at low temperatures writes [7]

$$L_K = \frac{h}{4e^2 k_F v_F W}$$

(1)

From these expressions one recovers the plasmon velocity $v_p = 1/\sqrt{L_K C}$ and the characteristic impedance $Z_\infty = \sqrt{L_K/C}$ of the plasmonic strip line. The line resistance $r = R/L$ accounts for plasmon losses which in principle include ohmic, viscous and dielectric contributions. The latter are negligible in our low-frequency range and viscous losses are minimized by using a plane wave geometry. Upon increasing the carrier density, the plasmonic response, with $L_K \propto 1/k_F$ (single layer graphene), takes over single particle diffusive response, with $r \propto 1/k_F^2$ (constant mobility), allowing for low-damping plasmon propagation. The crossover occurs whenever the total strip resistance $R \lesssim Z_\infty$, or equivalently the plasmon damping length $\alpha^{-1} \gtrsim L$. Dealing with a resonant
device, the PRC admittance, $Y = j\omega \times \text{tanh} \left[ \frac{L_{0}\sqrt{j\omega (r + jL_{K} \omega)}}{\sqrt{j\omega (r + jL_{K} \omega)}} \right]$, is conveniently cast into the compact form:

$$Y = Z_{\infty}^{-1} \times \frac{\tan \left( \frac{\sqrt{1 - 2j/Qf}}{\sqrt{1 - 2j/Qf}} \right)}{\sqrt{1 - 2j/Qf}},$$

(2)

where $f = \omega L_{0}\sqrt{L_{K} \omega}$ is the reduced frequency. The capacitive character of the resonator is encoded in the low-frequency response $Y/L = j\omega$. Equation (2) features a resonance behavior with a fundamental frequency at $f_{0} = \pi/2$, an admittance peak amplitude $\mathcal{Y}[Y(f_{0})] = Q/2\pi$ and a width $\Delta f \approx f_{0}/Q$. It includes higher harmonics, constituting the frequency comb $f_{k} = (2k + 1)f_{0}$ with $Q_{k} \sim (2k + 1)Q$. The latter are discarded here due to the finite 40 GHz bandwidth of our cryogenic setup.

The rise of a plasma resonance in increasing electron density is illustrated in figures 1(d)-(g). Admittance spectra, measured at $T = 30 \text{ K}$, have been obtained after deembedding a contact resistance $R_{c} = 43 \text{ Ohms}$. Such a low value was obtained by back-gating the capacitor access region. Data are presented together with their fits with equation (2) (dashed lines). At the lowest density the channel resistance takes over the kinetic inductance. The plasmon resonance

$f_{0} \sim 14 \text{ GHz}$ is overdamped with $Q \sim 0.4$ (figure 1(d)). The admittance spectrum is reminiscent of the evanescent wave response reported in [16-18]. Fingerprints of a resonant behavior become perceptible for $Q \approx 0.5$ with a shallow minimum of $\mathcal{Y}(Y)$ at $f \approx f_{0}$ (figure 1(e)). A genuine resonance develops at $n \gtrsim 1 \times 10^{12} \text{ cm}^{-2}$ (figure 1(f)) and culminates at $f_{0} \approx 38 \text{ GHz}$ with $Q = 1.69$ for $n = 2 \times 10^{12} \text{ cm}^{-2}$ (figure 1(g)). We deduce a plasmon velocity $v_{p} = 4f_{0}L_{0} = 3.6 \times 10^{8} \text{ m s}^{-1}$ in agreement with the above estimate based on geometry, and a plasmon damping length $\lambda_{\text{d}} = (2Q/\pi)L \approx 26 \mu\text{m}$. Plasmon losses correspond to a channel resistance $R = 40 \text{ Ohms}$ (figure 1(g)) approaching the characteristic impedance $Z_{\text{c}} = 35 \text{ Ohms}$, which is a suitable measuring condition. The same procedure has been reproduced by recording 400 complex admittance spectra covering the density and temperature ranges, $n = -0.1 \rightarrow 2.25 \times 10^{12} \text{ cm}^{-2}$ and $T = 10 \rightarrow 300 \text{ K}$, where we find a quality factor peaking to $Q \gtrsim 2$ at 10 K (inset of figure 2(a)). Figures 2(a), (b) summarize the doping dependence of the resonator parameters $v_{p}(n)$, $Z_{\infty}(n)$ obtained using the same fitting procedure. From these values we calculate $L_{K}(n)$, $C(n)$ (30 K data in figure 2(c)) and find a good agreement with the theoretical capacitance formula (black dashed line), including the dip of $C_{G}(n)$ at neutrality. Still, we observe a deviation of $L_{K}(n)$ from theory (blue dashed line) which exceeds our experimental uncertainties. This deviation is significant thanks to the increased accuracy of the resonant capacitor technique in the determination of $C$ and $L_{K}$ when compared to non-resonant techniques [7]. It is too large ($\pm 100 \text{ pH}$) to be explained by geometrical inductance effects ($\mu_{0}W \sim 10 \text{ pH}$) or systematic errors in the deembedding procedure ($\pm 20 \text{ pH}$ depending on frequency). From the channel resistance we estimate the conductivity and the mean free path $l_{\text{mf}}(n, T)$ which is plotted in (figure 2(d)) for typical temperatures. Mobility saturates near $\mu = 250 \text{ 000 cm}^{2} \text{ V}^{-1} \text{s}^{-1}$ at low temperatures (dashed black line in figure 2(d)). At high temperatures we find a mean free path plateau $l_{\text{mf}}(T) \sim 0.7 \times 300/T \mu\text{m}$, in agreement with theoretical estimates of the acoustic phonon limited resistivity [19].

To summarize, we have shown that the PRC principle works and provides an extensive characterization of equilibrium and transport graphene parameters including the compressibility $C_{G}(n, T)$, the kinetic inductance $L_{K}(n, T)$ and the mean-free-path $l_{\text{mf}}(n, T)$. The plasmon velocity matches expectations for the screened case. The weak doping dependencies of the plasmon velocity and characteristic impedance in figures 2(a), (b) reflect theoretical expectations for massless graphene where $v_{p}, Z_{\infty} \sim n^{-\frac{3}{2}}$ as opposed to $v_{p} \sim n^{-\frac{1}{2}}$ for massive 2DESs such as bilayer graphene. The deviation from theory, observed in the inductance, gives rise to a saturation of the plasmon velocity $v_{p} \lesssim 4v_{f}$ and characteristic impedance $Z_{\infty} \gtrsim 35 \text{ Ohms}$. A tentative explanation for this discrepancy is an additive mass contribution from the dilute 2DES in the back-gated silicon substrate, which loads graphene Dirac plasmons according to its capacitive coupling to graphene electrons, and eventually restricts electron mobility. Such a residual substrate coupling can easily be avoided by substituting the silicon back gate with a metallic bottom gate following references [14, 20].

In conclusion, we have demonstrated a graphene PRC with a resonant frequency $f_{0} \approx 40 \text{ GHz}$ and a quality factor $Q \approx 2$. Quality factors remain smaller than the $Q \approx 130$ reported in the ultrashort wavelength ($\lambda_{p} = 0.1 \rightarrow 0.2 \mu\text{m}$) MIR domain of [5]. However, the GHz damping length (26 $\mu\text{m}$) is comparable to the MIR value (10 $\mu\text{m}$ in [5]), which is promising for applications. We have measured the doping dependence of plasmon velocity, line capacitance and kinetic inductance in good agreement with theory beside a small shift of the kinetic inductance. Our experiment paves the way to active plasma resonance transistors working in the $0.1 \rightarrow 1 \text{ THZ}$ domain, above the natural cutoff $\sim 0.1 \text{ THZ}$ of conventional graphene field-effect transistors [21, 22]. Building on this first demonstration performed at cryogenic temperatures, a room temperature variant can be envisioned by scaling down the sample size and the plasmon wave length by a factor 10 to accommodate the phonon-limited mean free path of 0.7 $\mu\text{m}$ at 300 K. During the reviewing process, we became aware of a related work [23] demonstrating the resonant detection of THZ radiation using graphene plasmons. These achievements might in particular lead to the conception of novel detectors in the 600 GHz frequency domain, highly desirable for
air-craft RADARs operating in the mm-range, with a resolution ultimately limited by hot electron effects [14, 24, 25]. The long plasmonic channels are compatible with the incorporation of bottom gate arrays to engineer doping modulation profiles [26] and investigate the propagation of Dirac plasmons in bipolar superlattices.

Methods

Micromechanical exfoliation provides a pristine monolayer graphene, which is subsequently encapsulated between two layers of hexagonal boron nitride (hBN) in order to achieve a high electronic mobility (phonon limited at room temperature). The encapsulation is performed by means of a dry pick-up technique using a polyvinyl alcohol (PVA) and polymethylmethacrylate (PMMA) stamp on a polydimethylsiloxane support [8]. A top hBN flake (10–30 nm thick) is transferred from its substrate to the PMMA. Then the graphene is picked up by the first hBN flake thanks to the strong van der Waals interactions and deposited on a bottom hBN flake, which was previously exfoliated onto a high resistivity silicon (with SiO₂) substrate. The transfer process is carried out using a custom-made alignment system with a heating plate operating between 30 °C and 130 °C.

Finally, the PVA and PMMA polymers are dissolved in hot water (95 °C) and acetone, respectively.

The encapsulated graphene samples are generally hundreds of μm² in size and need to be patterned into a passive circuit. After characterization by Raman spectroscopy (figure 3(c)) and atomic force microscopy (AFM, figure 3(a)), we used e-beam nanolithography to define a T-shape capacitor (figure 3(b)). The length of the channel, according to its mobility, defines the quarter wave plasma resonance and needs to be long enough to obtain a signal in the

Figure 2. Density and temperature dependence of the graphene plasma resonance capacitor (PRC) deduced from three-parameter theoretical fits of the admittance spectra with equation (2).

(a) Density dependence of the plasmon velocity at $T = 30$ K, deduced from the resonant frequency $v_p = 4L_\omega$. The dashed line is the theoretical expectation of equation (1) for the low temperature limit. Inset, quality factor: density dependence at 30 K (black), temperature dependence at $2 \times 10^{12}$ cm$^{-2}$ (red). (b) Density dependence of the plasmonic line characteristic impedance ($T = 30$ K); dashed line is the theoretical prediction. (c) Density dependence of the capacitance (red dots) and kinetic inductivity (blue dots) $C_p W$ ($T = 30$ K). Black and blue dashed lines are the low-temperature theoretical expectations for the capacitance and inductivity $C_p W$. (d) Density dependence of the electronic mean-free-path $l_{\text{mp}}$ for a representative set of temperatures. $l_{\text{mp}}$ saturates at low temperatures to a constant mobility regime $l_{\text{mp}} = \mu l_k T / e$ with $\mu \approx 250 000$ cm$^{-1}$ V$^{-1}$ s$^{-1}$ (black dashed line). At high temperatures, we retrieve the acoustic-phonon-limited scattering length plateau $l_{\text{mp}} \sim 0.7 \times (300/T) \mu$m.
0–40 GHz bandwidth. The etching of the hBN-graphene-hBN sandwich was performed using a mixture of 
CHF3/O2 plasma etching through a temporary 40 nm thick aluminum mask. A chromium/gold (5/200 nm) edge 
contact was then deposited on the source edge of the T-shape heterostructures (using a comb design to enhance the 
contact length and reduce the contact resistance). In order to passivate the other edges of the heterostructures and to 
avoid any source-gate leakage current in the PRC, we oxidized 2 nm of aluminum followed by 10 nm of Al2O3 by 
atomic layer deposition. Finally, a chromium/gold gate electrode was deposited on top and the PRC was embedded 
into a CPW. Similarly, thruline and dummy reference structures were defined on the same chip for de-embedding 
(see below).

High frequency admittance measurements were carried out in a Janis cryogenic probe station in the 
temperature range T = 10–300 K. The two-port scattering parameters Sij of the capacitor were measured using 
an Anritsu MS4644B VNA in the 0–40 GHz range. Bias tees were used to decouple the DC gate voltages from the 
GHz probe signal. A short-open-load-reciprocal protocol was used to calibrate the wave propagation until the 
probe tips. We then measured S parameters of a symmetric thruline reference structure, calculated its Aabcd 
cascade matrix 

\[ A_{thru} \] 

and took the inverse of the square root of this matrix 

\[ A_{thru}^{-1/2} \] 

. The wave propagation in the 

coplanar access of the PRC can now be de-embedded from its Aabcd matrix:

\[ A_{PPC}^{-1/2} \cdot A_{thru}^{-1/2} \]

. The same procedure was carried out on a dummy reference structure which has the same contact and gate 
geometry as the PRC but does not contain encapsulated graphene. Finally, the Aabcd matrices of the PRC and 
the dummy structure were converted to admittance (Y) parameters and the Y matrix of the dummy structure 
was subtracted from that of the PRC in order to de-embed remaining stray capacitances. The Yij parameters 
should now all be the same (except for a minus sign in front of the off-diagonal elements), due to the symmetry 
of our two-port network. The admittance data shown in this article correspond to one of the off-diagonal 
elements, −Y12, which was further de-embedded from the contact resistance: 

\[ Y = (-1/Y_{12} - R_c)^{-1} \]

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Figure 3. Fabrication process of a plasma resonance capacitor (PRC). (a) AFM image of the hBN/graphene/hBN stack deposited on 
the high-resistivity SiO2/Si substrate. The dashed and solid lines show the contours of the pristine graphene flake and targeted PRC 
sample. (b) Optical image of the PRC sample after lithography, before etching. (c) Map of the Raman 2D-peak width (color encoded in 
the range 10–30 cm−1) showing the good sample homogeneity and highlighting the presence of a spurious fold and bubble in this 
sample (PRC7).
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