Cross-Checking Different Sources of Mobility Information

Maxime Lenormand1*, Miguel Picornell2, Oliva G. Cantú-Ros2, Antònia Tugores1, Thomas Louail1,4, Ricardo Herranz2, Marc Barthelemy3,5, Enrique Frías-Martínez6, José J. Ramasco1

1 Instituto de Física Interdisciplinar y Sistemas Complejos IFISC (CSIC-UIB), Palma de Mallorca, Spain, 2 Nommon Solutions and Technologies, Madrid, Spain, 3 Institut de Physique Théorique, CEA-CNRS (URA 2306), Gif-sur-Yvette, France, 4 Geographe-Citées, CNRS-Paris 1-Paris 7 (UMR 8504), Paris, France, 5 Centre d’Analyse et de Mathématiques Sociales, EHESS-CNRS (UMR 8557), Paris, France, 6 Telefonica Research, Madrid, Spain

Abstract

The pervasive use of new mobile devices has allowed a better characterization in space and time of human concentrations and mobility in general. Besides its theoretical interest, describing mobility is of great importance for a number of practical applications ranging from the forecast of disease spreading to the design of new spaces in urban environments. While classical data sources, such as surveys or census, have a limited level of geographical resolution (e.g., districts, municipalities, counties are typically used) or are restricted to generic workdays or weekends, the data coming from mobile devices can be precisely located both in time and space. Most previous works have used a single data source to study human mobility patterns. Here we perform instead a cross-check analysis by comparing results obtained with data collected from three different sources: Twitter, census, and cell phones. The analysis is focused on the urban areas of Barcelona and Madrid, for which data of the three types is available. We assess the correlation between the datasets on different aspects: the spatial distribution of people concentration, the temporal evolution of people density, and the mobility patterns of individuals. Our results show that the three data sources are providing comparable information. Even though the representativeness of Twitter geolocated data is lower than that of mobile phone and census data, the correlations between the population density profiles and mobility patterns detected by the three datasets are close to one in a grid with cells of 2×2 and 1×1 square kilometers. This level of correlation supports the feasibility of interchanging the three data sources at the spatio-temporal scales considered.

Introduction

The strong penetration of ICT tools in the society’s daily life is opening new opportunities for the research in socio-technical systems [1–3]. Users’ interactions with or through mobile devices get registered allowing a detailed description of social interactions and mobility patterns. The sheer size of these datasets opens the door to a systematic statistical treatment while searching for new information. Some examples include the analysis of the structure of (online) social networks [4–13], human cognitive limitations [14], information diffusion and social contagion [15–19], the role played by social groups [12,17], language coexistence [20] or even how political movements raise and develop [21–23].

The analysis of human mobility is another aspect to which the wealth of new data has notably contributed [24–28]. Statistical characteristics of mobility patterns have been studied, for instance, in Refs. [24,25], finding a heavy-tail decay in the distribution of displacement lengths across users. Most of the trips are short in everyday mobility, but some are extraordinarily long. Besides, the travels are not directed symmetrically in space but show a particular radius of gyration [25]. The duration of stay in each location also shows a skewed distribution with a few preferred places clearly ranking on the top of the list, typically corresponding to home and work [26]. All the insights gained in mobility, together with realistic data, have been used as proxies for modeling the way in which viruses spread among people [29] or among electronic devices [30]. Recently, geolocated data has been also used to analyze the structure of urban areas [31–38], the relation between different cities [39] or even between countries [40].

Most mobility and urban studies have been performed using data coming essentially from a single data source such as: cell phone data [5,11,25,26,28,30–38], geolocated tweets [20–22,40], census-like surveys or commercial information [29]. There is only a few recent exceptions, for instance, epidemic spreading studies [41]. When the data has not been generated or gathered ad hoc to
address a specific question, one fair doubt is how much the results are biased by the data source used. In this work, we compare spatial and temporal population density distributions and mobility patterns in the form of Origin-Destination (OD) matrices obtained from three different data sources for the metropolitan areas of Barcelona and Madrid. This comparison will allow to discern whether or not the results are source dependent. In the first part of the paper the datasets and the methods used to extract the OD tables are described. In the second part of the paper, we present the results. First, a comparison of the spatial distribution of users according to the hour of the day and the day of the week showing that both Twitter and cell phone data are highly correlated on this aspect. Then, we compare the temporal distribution of users by identifying where people are located according to the hour of the day, we show that the temporal distribution patterns obtained with the Twitter and the cell phone datasets are very similar. Finally, we compare the mobility networks (OD matrices) obtained from cell phone data, Twitter and census. We show that it is possible to extract similar patterns from all datasets, keeping always in mind the different resolution limits that each information source may inherently have.

Materials and Methods

This work is focused on two cities: the metropolitan areas of Barcelona [42] and Madrid [43] both in Spain and for which data from the three considered sources is available. The metropolitan area of Barcelona contains a population of 3,218,071 (2009) within an area of 636 km². The population of the metropolitan area of Madrid is larger, with 5,512,495 inhabitants (2009) within an area of 1,935 km² [44]. In order to compare activity and intra mobility in each city, the metropolitan areas are divided into a regular grid of square cells of lateral size \( l \) (Figure 1b). Two different sizes of grid cells \( l = 1 \text{ km} \) and \( l = 2 \text{ km} \) are considered in order to evaluate the robustness of the results. Since mobility habits and population concentration may change along the week, we have divided the data into four groups: one, from Monday to Thursday, another one between 6pm and 9pm. They also show that the Twitter and cell phone data are highly correlated on this aspect. Then, we compare the temporal distribution of users by identifying where people are located according to the hour of the day, we show that the temporal distribution patterns obtained with the Twitter and the cell phone datasets are very similar. Finally, we compare the mobility networks (OD matrices) obtained from cell phone data, Twitter and census. We show that it is possible to extract similar patterns from all datasets, keeping always in mind the different resolution limits that each information source may inherently have.

1.2 Twitter data

The dataset comprehends geolocated tweets of 27,707 users in Barcelona and 50,272 in Madrid in the time period going from September 2012 to December 2013. These users were selected because it was detected from the general data streaming with the Twitter API [45] that they have emitted at least a geolocated tweet from one of the two cities. Later, as a way to increase the quality of our database, a specific search over their most recent tweets was carried out [46]. As for the cell phone data, the number of Twitter users \( T_{v,w,h} \) in each grid cell \( g \) per hour \( h \) were computed for each day group \( w \). The number of mobile phone users per day for the two metropolitan areas as a function of the time of day, and according to the day group, are displayed in Figure 2. The curves in Figure 2a show two peaks, one between noon and 3pm and another one between 6pm and 9pm. They also show that the number of mobile phone users is higher during weekdays than during the weekends. The same curve is obtained for Madrid with about twice the number of users with respect to Barcelona. Further details about the data pre-processing are given in Supporting Information S1 (Section Mobile phone data pre-processing, Figure S1 and Figure S2).

In order to extract OD matrices from the cell phone calls a subset of users, with a mobility reliably recoverable, was selected. For this analysis we only consider commuting patterns in workdays. The users’ home and work are identified as the Voronoi cell most frequently visited on weekdays by each user between 8 pm and 7 am (home) and between 9 am and 5 pm (work). We assume that there must be a daily travel between home and work location of each individual. Users with calls in more than 40% of the days under study at home or work are considered valid. Aggregating the complete flow over users, an OD commuting matrix is obtained containing in each element the flow of people traveling between a Voronoi cell of residence and another of work. Since the Voronoi areas do not exactly match the grid cells, a transition matrix to change the scale is employed (see Supporting Information S1 for details).

1.1 Mobile phone data

The cell phone data that we are analyzing come from anonymized users’ call records collected during 55 days (noted as \( D \) hereafter) between September and November 2009. The call records are registered by communication towers (Base Transceiver Station or BTS), identified each by its location coordinates. The area covered by each tower can be approximated by a Voronoi tessellation of the urban areas, as shown in Figure 1a for Barcelona. Each call originated or received by a user and served by a BTS is thus assigned to the corresponding BTS Voronoi area. In order to estimate the number of people in different areas per period of time, we use the following criteria: each person counts only once per hour. If a user is detected in \( k \) different positions within a certain 1-hour time period, each registered position will count as \((1/k)\) “units of activity”. From such aggregated data, activity per zone and per hour is calculated. Consider a generic grid cell \( g \) for a day \( d \) and hour between \( h \) and \( h+1 \), the \( m \) Voronoi areas intersecting \( g \) are found and the number of mobile phone users \( P_{g,d,h} \) is calculated as follows:

\[
P_{g,d,h} = \sum_{i=1}^{m} N_{i,d,h} \frac{A_{v_i \cap g}}{A_i},
\]

where \( N_{i,d,h} \) is the number of users in a Voronoi cell \( v \) on day \( d \) at time \( h \), \( A_{v \cap g} \) is the area of the intersection between \( v \) and \( g \), and \( A_v \) the area of \( v \). The \( D \) days available in the database are then divided in four groups according to the classification explained above and the average number of mobile phone users for each day group \( w \) is computed as

\[
P_{g,w,h} = \frac{\sum_{D \in D_w} P_{g,d,h}}{|D_w|}.
\]
much from weekdays to weekend days. Moreover, we can observe that the number of Twitter users is higher during the second peak than during the first one.

The identification of the OD commuting matrices using Twitter is similar to the one explained for the mobile phones except for two aspects. Since the number of geolocated tweets is much lower than the equivalent in calls per user, the threshold for considering a user valid is set at 100 tweets on weekdays in all the dataset. The other difference is that since the tweets are geolocated with latitude and longitude coordinates, the assignment to the grid cells is done
directly without the need of intermediate steps through the Voronoi cells. As for the phone, we keep only users working and living within the metropolitan areas.

1.3 Census data
The Spanish census survey of 2011 included a question referring to the municipality of work of each interviewed individual. This survey has been conducted among one-fifth of the population. This information, along with the municipality of the household where the interview was carried out, allows for the definition of OD flow matrices at the municipal level [44]. For privacy reasons, flows with a number of commuters lower than 10 have been removed. The metropolitan area of Barcelona is composed of 36 municipalities, while the one of Madrid contains 27 municipalities. In addition to the flows, we have obtained the GIS files with the border of each municipality from the census office. This information is used to map the OD matrices from Twitter or the cell phone data to this more coarse-grained spatial scale to compare mobility patterns across datasets.

1.4 Ethics statement
This work includes the use of users’ geolocated information. Since we are interested only in statistical features and not in individual traits of users, all the data have been anonymized and aggregated before the analysis that has been performed in accordance with all local data protection laws. Twitter and Census data are obtained from public sources as explained above. The cell phone data is proprietary and subject to strict privacy regulations. The access to this dataset was granted after reaching a non-disclosure agreement with the proprietary, who anonymized and aggregated the original data before giving access to other authors.

Figure 3. Correlation between the spatial distribution of Twitter users and mobile phone users for the weekdays (aggregation from Monday to Thursday) and from noon to 1pm for the metropolitan area of Barcelona ($l=2$ km). (a) Scatter-plot composed by each pair ($T_{g,w}, P_{g,w}$), the values have been normalized (dividing by the total number of users) in order to obtain values between 0 and 1. The red line represents the perfect linear fit with slope equal to 1 and intercept equal to 0. (b)–(c) Spatial distribution of Twitter users (b) and mobile phone users (c). In order to facilitate the comparison of both distributions on the map, the proportion of users in each cell is shown (always bounded in the interval $[0, 1]$).

doi:10.1371/journal.pone.0105184.g003

Figure 4. Box-plots of the Pearson correlation coefficients obtained for different hours between $T$ and $P$ (from the left to the right: the weekdays (aggregation from Monday to Thursday), Friday, Saturday and Sunday). The blue boxes represent Barcelona. The green boxes represent Madrid. (a) $l=2$ km. (b) $l=1$ km.

doi:10.1371/journal.pone.0105184.g004
Results

2.1 Spatial distribution

A first question to address is how much the human activity level is similar or not when estimated from Twitter, $T$, or from cell phone data $P$ across the urban space in grid cells of 2 by 2 km. To quantify similarity, we start by depicting in Figure 3 a scatter plot composed by each pair $(T_{g,w,h}, P_{g,w,h})$ for every grid cell of the metropolitan area of Barcelona taking $w$ as the weekdays (aggregation from Monday to Thursday). The hour $h$ is set from midday to 1pm. A first visual inspection tells us that the agreement between the activity inferred from each dataset is quite good. In fact, the Pearson correlation coefficient between the two estimators of activity is of $\rho = 0.96$. Furthermore, the portion of activity can...
be depicted on two maps as in Figure 3b and c. The similarity of the areas of concentration of the activity is patent.

More systematically, we plot in Figure 4a, the box-plots of the Pearson correlation coefficients for each day group and both case studies as observed for different hours. We obtain in average a correlation of 0.93 for Barcelona and 0.89 for Madrid. Globally, the correlation coefficients have higher value for Barcelona than for Madrid probably because the metropolitan area of Madrid is about four times larger than the one of Barcelona. It is interesting to note that the average correlation remains high even if we increase the resolution by using a value of $l=1$ km. Indeed, we obtain in average a correlation of 0.85 for Barcelona and 0.83 for Madrid at that new scale (Figure 4b).

2.2 Temporal distribution

After the spatial distribution of activity, we investigate the correlation between the temporal activity patterns as observed from each grid cell. We start by normalizing $T$ and $P$ such that the total number of users at a given time on a given day is equal to 1:

$$T_{g,0, w, h} = \frac{T_{g,0, w, h}}{\sum_{g=1}^{n} T_{g, w, h}}, \quad P_{g,0, w, h} = \frac{P_{g,0, w, h}}{\sum_{g=1}^{n} P_{g, w, h}}.$$ (3)

This normalization allows for a direct comparison between sources with different absolute user’s activity. For a given grid cell $g=g_0$, we defined the temporal distribution of users $P_{g_0}$ as the

concatenation of the temporal distribution of users associated with each day group. For each grid cell we obtained a temporal distribution of users represented by a vector of length 96 corresponding to the 4x24 hours.

After removing cells with zero temporal distribution, cells of common temporal profiles were found using the ascending hierarchical clustering (AHC) method. The average linkage clustering and the Pearson correlation coefficient were taken as agglomeration method and similarity metric, respectively [47]. We have also implemented the k-means algorithm for extracting clusters but better silhouette index values were obtained with the AHC algorithm (see details in Figure S3 in Supporting Information S1). To choose the number of clusters, we used the average silhouette index $S$ [48]. For each cell $g$, we can compute $a(g)$ the average dissimilarity of $g$ (based on the Pearson correlation coefficient in our case) with all the other cells in the cluster to which $g$ belongs. In the same way, we can compute the average dissimilarities of $g$ to the other clusters and define $b(g)$ as the lowest average dissimilarity among them. Using these two quantities, we compute the silhouette index $s(g)$ defined as

$$s(g) = \frac{b(g) - a(g)}{\max\{a(g), b(g)\}},$$ (4)

which measures how well clustered $g$ is. This measure is comprised between $-1$ for a very poor clustering quality and 1 for an appropriately clustered $g$. We choose the number of clusters that maximize the average silhouette index over all the grid cells $S=\sum_{g=1}^{n} s(g)/n$.

For the mobile phone data, three clusters were found with an average silhouette index equal to 0.38 for Barcelona and to 0.43

Figure 6. Comparison between the non-zero flows obtained with the Twitter dataset and the mobile phone dataset (the values have been normalized by the total number of commuters for both OD tables). The points are scatter plot for each pair of grid cells. The red line represents the $x=y$ line. (a) Barcelona. (b) Madrid. In both cases $l=2$ km.

doi:10.1371/journal.pone.0105184.g006
for Madrid. The three temporal distribution patterns of mobile phone users are shown in Figure 5 for Barcelona. These three clusters can be associated with the following land uses:

- **Business**: this cluster is characterized by a higher activity during the weekdays than the weekend days. In Figure 5a, we observe that the activity takes place between 6 am and 3 pm with a higher activity during the morning.

- **Residential**: this cluster is characterized by a higher activity during the weekend days than during the weekdays. Figure 5c shows that the activity is almost constant from 9 am during the weekend days. During the weekdays we observe two peaks, the first one between 7 am and 8 am and the second one during the evening.

- **Nightlife**: this cluster is characterized by a high activity during the night especially the weekend (Figure 5e).

It is remarkable to note that we obtain the same three patterns for Madrid and that these patterns are robust for different values of the scale parameter $l$ (see details in Figure S4, S5 and S6 in Supporting Information S1).

For Twitter data, considering a number of clusters smaller than 10, silhouette index values lower than 0.1 are obtained for both case studies. These low values mean that no clusters have been detected in the data probably because the Twitter data are too noisy. A way to bypass this limitation is to check if, for both data sources, the same patterns are obtained considering the different clusters obtained with the mobile phone data. To do so the temporal distribution patterns of Twitter users associated with the three clusters obtained with the mobile phone data are computed. We note in Figure 5 that for Barcelona the temporal distribution patterns obtained with the Twitter data are very similar to those obtained with the mobile phone data. We obtain the same correlation for Madrid and for different values of the scale $l$ (see details in Figure S4, S5 and S6 in Supporting Information S1).
2.3 Users’ mobility

In this section, we study the similarity between the OD matrices extracted from Twitter and cell phone data. As it involves a change of spatial resolution needing extra attention, the comparison with the census is relegated to a coming section. We are able to infer for the metropolitan areas of Barcelona and Madrid the number of individuals living in the cell \( i \) and working in the cell \( j \).

Figure 6 shows a scattered plot with the comparison between the flows obtained in the OD matrices for links present in both networks. In order to compare the two networks, the values have been normalized by the total number of commuters.

The overall agreement is good, the Pearson correlation coefficient is around \( r \approx 0.9 \). This coefficient measures the strength of the linear relationship between the normalized flows extracted from both networks, including the zero flows (i.e. flows with zero commuters). However, a high correlation value is not sufficient to assess the goodness of fit. Since we are estimating the fraction of commuters on each link, the values obtained from Twitter and the cell phone data should be ideally not only linearly related but the same. That is, if \( y \) if the estimated fraction of mobile phone users on a connection and \( x \) the estimated Twitter users on the same link, there should be not only a linear relation, which involves a high Pearson correlation, but also \( y = x \). It is, therefore, important to verify that the slope of the relationship is equal to one. To do so, the coefficients of determination \( R^2 \) are computed to measure how well the scatterplot is fitted by the curve \( y = x \). Since there is no particular preference for any set of data as \( x \) or \( y \), two coefficients \( R^2 \) can be measured, one using Twitter data as the independent

![Figure 8. Commuting distance distribution obtained with both datasets.](https://doi.org/10.1371/journal.pone.0105184.g008)

![Figure 9. Comparison between the non-zero flows obtained with the three datasets for the Barcelona’s case study (the values have been normalized by the total number of commuters for both OD tables).](https://doi.org/10.1371/journal.pone.0105184.g009)
variable $x$ and another using cell phone data. Note that if the slope of the relationship is strictly equal to one the two $R^2$ must be equal to the square of the correlation coefficient, we obtain a value around $R^2 = 0.85$ for Barcelona and around 0.81 for Madrid. The slope of the best fit is in both cases very close to one.

The dispersion in the points is higher in low flow links. This can be explained by the stronger role played by the statistical fluctuations in low traffic numbers. Moreover, if we increase the resolution by using a value of $l$ equal to 1 km, the Pearson correlation coefficient remains high with a value around 0.8 (see details in Figure S7 in Supporting Information S1). The extreme situation of these fluctuations occurs when a link is present in one network and it has zero flow in the other (missing links). On average 90% of these links have a number of commuters equal to one in the network in which they are present. This shows that the two networks are not only inferring the same mobility patterns, but that the information left outside in the cross-check corresponds to the weakest links in the system. In order to assess the relevance of the missing links, the weight distributions of these links is displayed in Figure 7 for all the networks and case studies. As a comparison line, the weight distribution of all the links are also shown in the different panels. In all cases, the missing links have flows at least one order of magnitude, sometimes two orders, lower than the strongest links in the corresponding networks. To be more precise, the strongest flow of the missing links is, depending on the case, between 25 and 464 times lower than the highest weight of all the links. Furthermore, the average weight of the missing links is between 4 and 9 times lower than that obtained over all the links. Most of the missing links are therefore negligible in the general network picture.

With the aim of going a little further, we analyze and compare next the distance distribution for the trips obtained from both datasets. The geographical distance along each link in the OD matrices is calculated and the number of people traveling in the links is taken into account to evaluate the travel-length distribution. Figure 8 shows these distributions for each network. Strong similarity between the two distributions can be observed in the two cities considered.

### 2.4 Census, Twitter and cell phone

As a final cross-validation, we compare the OD matrices estimated in workdays from Twitter and cell phone data to those extracted from the 2011 census in Barcelona and Madrid. The census data is at the municipal level, which implies that to be able to perform the comparative analysis the geographical scale of both Twitter and phone data must be modified. To this end, the GIS files with the border of each municipality were used, instead of the grid, to compute the OD matrices from Twitter and cell phone data. Figure 9 shows a scattered plot with the comparison between the flows obtained with the three networks. A good agreement between the three datasets is obtained with a Pearson correlation close to 0.9 in the two cities analyzed. The second aspect considered has been the temporal distribution of individuals which allow us to determine the type of activity that are most common in specific urban areas. We show that similar temporal distribution patterns can be extracted from both Twitter and cell phone datasets. The last question studied has been the extraction of mobility networks in the shape of Origin-Destination commuting matrices. We observe that at high spatial resolution, in grid cells with sides of 1 or 2 km, the networks obtained with both cell phones and Twitter are comparable. Of course, the integration time needed for Twitter is higher in order to obtain similar results. Twitter data can run in serious problems too if instead of recurrent mobility the focus is on shorter term mobility, but this point falls beyond the scope of this work. Finally, the comparison with census data is also acceptable: both Twitter and cell phone data reproduce the commuting networks at the municipal scale from an overall perspective. Still and although good on average, the agreement between the three different datasets is broken in some particular connections that deviate from the diagonal in our scatterplots. This can be explained by the fact that the datasets come from different sources, were collected in different years and may have different biases and level of representativeness. For example, Twitter is supposed to be used more by younger people. The explanation of these deviations and whether they are just stochastic fluctuations or follow some rationale could be an interesting avenue for further research.

These results set a basis for the reliability of previous works basing their analysis on single datasets. Similarly, the door to extract conclusions from data coming from a single data source (due to convenience of facility of access) is open as long as the spatio-temporal scales tested here are respected.

### Supporting Information

**Supporting Information S1**  [Supporting files and figures.](#)

**Author Contributions**

Conceived and designed the experiments: ML, JR OGC MP. Performed the experiments: ML, JR OGC MP. Analyzed the data: ML, JR OGC MP. Contributed reagents/materials/analysis tools: ML, JR OGC MP, AT RH EFM TL MB. Contributed to the writing of the manuscript: ML, JR OGC MP, AT RH EFM TL MB.
References

1. Watts DJ (2007) A twenty-first century science. Nature 445: 489.
2. Lazer D, Pentland A, Adamic L, Aral S, Barabasi AL, et al. (2009) Computational social science. Science 323: 721.
3. Vespignani A (2009) Predicting the behavior of techno-social systems. Science 325: 425–428.
4. Liben-Nowell D, Novak J, Kumar R, Raghavan P, Tomkins A (2005) Geographic routing in social networks. Proc Natl Acad Sci USA 102: 11623–11628.
5. Onnela JP, Saramaki J, Hyvonen J, Szabo G, Lazer D, et al. (2007) Structure and tie strengths in mobile communication networks. Proc Natl Acad Sci USA 104: 7332–7336.
6. Jin A, Song X, Finin T, Tseng B (2007) Why we Twitter: understanding microblogging usage and communities. Proc. 9th WEBKDD and 1st SNA-KDD 2007.
7. Huberman BA, Romero DM, Wu F (2008) Social networks that matter: Twitter under the microscope. First Monday 14.
8. Krishnamurthy B, Gill P, Arlitt M (2008) A few chirps about Twitter. Proc. WOSP'08.
9. Lewis K, Kossinjsanin A, Gonzalez M, Wimmer A, Christakis N (2008) Tastes, ties and time: a new social network dataset using Facebook.com. Social Networks 30: 330–340.
10. Millovo A, Koppula HS, Gummadi KP, Druschel P, Bhatapadhyee B (2008) Growth of the flickr social network. Proceedings of the first workshop on Online Social Networks – WOSPO8, pp. 25–30.
11. Eagle N, Pentland AS, Lazer D (2009) From the Cover: Inferring friendship network structure by using mobile phone data. Proc Natl Acad Sci USA 106: 15274–15279.
12. Ferrara E (2012) A large-scale community structure analysis in Facebook. EPJ Data Science 1: 9.
13. Grabowicz PA, Ramasco JJ, Goncalves B, Eguiluz VM (2013) Entangling the dynamics of the news cycle. Proceedings of the 15th ACM SIGKDD international conference on knowledge discovery and data mining – KDD’09, p. 497–506.
14. Lehmann J, Goncalves B, Ramasco JJ, Cattuto C (2012) Dynamical classes of collective attention in Twitter. Proceedings of the 21st international conference on World Wide Web – WWW’12, pp. 251–260.
15. Leskovec J, Backstrom L, Kleinberg J (2009) Meme-tracking and the dynamics of the news cycle. Proceedings of the 15th ACM SIGKDD international conference on knowledge discovery and data mining – KDD’09, p. 497–506.
16. Bakhshi E, Rosem I, Marlow C, Adamic L (2012) The role of social networks in information diffusion. Proceedings of the 21st international conference on World Wide Web – WWW’12, pp. 519–528.
17. Grabowicz PA, Ramasco JJ, More E, Eguiluz VM (2012) Social features of online networks: the strength of intermediary ties in online social media. PLoS ONE 7: e29358.
18. Balcan D, Colizza V, Goncalves B, Ramasco JJ, Hidalgo CA, Barabasi AL (2009) Understanding the spreading patterns of mobile phone viruses. Science 324: 1071–1076.
19. Weng P, Gonzalez MC, Hidalgo CA, Barabasi AL (2009) Understanding the spreading patterns of mobile phone viruses. Science 324: 1071–1076.
20. Ratti C, Pulcelli RM, Williams S, Frenchman D (2006) Mobile landscapes: using location data from cell phones for urban analysis. Environment and Planning B: Planning and Design 32: 727–748.
21. Reades J, Calabrese F, Seltuk A, Ratti C (2017) Cellular census: Explorations in mobile phone data collection. Pervasive Computing, IEEE 6: 30–38.
22. Video S, Frias-Martinez E (2011) Robust land use characterization of urban landscapes using cell phone data. In: Proceedings of the 1st Workshop on Pervasive Urban Applications, in conjunction with 9th Int. Conf. Pervasive Computing.
23. Frias-Martinez V, Soto V, Hohwald H, Frias-Martinez E (2012) Characterizing urban landscapes using geolocated tweets. In: SocialCom/PASSAT. IEEE, pp. 239–246.
24. Isaacman S, Becker R, Caceres R, Martonosi M, Rowland J, et al. (2012) Human mobility modeling at metropolitan scales. In: Proceedings of the International Conference on Mobile Systems, Applications, and Services (MobiSys). ACM, pp. 239–252.
25. Toole JI, Ulm M, Bauer D, Gonzalez MC (2012) Inference land use from mobile phone activity. In: ACM Ubicomp2012.
26. Pei T, Sobolevsky S, Ratti C, Shaw SL, Zhou C (2013) A new insight into land use classification based on aggregated mobile phone data. ArXiv e-print arXiv:1310.6129.
27. Louail T, Lenormand M, Garcia-Canti O, Picornell M, Herranz R, et al. (2014) From mobile phone data to the spatial structure of cities. ArXiv e-print arXiv:1401.5450.
28. Noula A, Scellato S, Lambiotte R, Poniti M, Mascolo C (2012) A tale of many cities: Universal patterns in human urban mobility. PLoS ONE 7: e37027.
29. Havelka B, Siklo I, Beinat E, Sobolevsky S, Kazakopoulos P, et al. (2013) Geolocated twitter as a proxy for global mobility patterns. ArXiv e-print arXiv:1311.0680.
30. Lounis T, Lenormand M, Garcia-Canti O, Picornell M, Herranz R, et al. (2014) From mobile phone data to the spatial structure of cities. ArXiv e-print arXiv:1401.5450.
31. Área Metropolitana de Barcelona (nd) see "Atlas de la Comunidad de Madrid en el siglo XXI".
32. Área Metropolitana de Barcelona (nd) see "Atlas de la Comunidad de Madrid en el siglo XXI"
33. Balcan D, Colizza V, Goncalves B, Hu H, Ramasco JJ, et al. (2009) Multiscale mobility networks and the spatial spreading of infectious diseases. Proc Natl Acad Sci USA 106: 21484–21489.
34. Phithakkitnukoon S, Smoreda Z, Olivier P (2012) Socio-geography of human mobility: A study using longitudinal mobile phone data. PLoS ONE 7: e92935.
35. Isaacsman S, Becker R, García C, Martonosi M, Rowland J, et al. (2012) Human mobility modeling at metropolitan scales. In: Proceedings of the International Conference on Mobile Systems, Applications, and Services (MobiSys). ACM, pp. 239–252.
36. Toole JI, Ulm M, Bauer D, Gonzalez MC (2012) Inference land use from mobile phone activity. In: ACM Ubicomp2012.
37. Pei T, Sobolevsky S, Ratti C, Shaw SL, Zhou C (2013) A new insight into land use classification based on aggregated mobile phone data. ArXiv e-print arXiv:1310.6129.
38. Louail T, Lenormand M, Garcia-Canti O, Picornell M, Herranz R, et al. (2014) From mobile phone data to the spatial structure of cities. ArXiv e-print arXiv:1401.5450.
39. Noula A, Scellato S, Lambiotte R, Poniti M, Mascolo C (2012) A tale of many cities: Universal patterns in human urban mobility. PLoS ONE 7: e37027.
40. Havelka B, Siklo I, Beinat E, Sobolevsky S, Kazakopoulos P, et al. (2013) Geo-located twitter as a proxy for global mobility patterns. ArXiv e-print arXiv:1311.0680.
41. Tizzoni M, Bajardi P, Decuypere A, Kon Kam King G, Schneider CM, et al. (2013) On the use of human mobility proxy for the modeling of epidemics. ArXiv e-print arXiv:1309.2727.
42. Área Metropolitana de Barcelona (nd) see "Atlas de la Comunidad de Madrid en el siglo XXI".
43. Instituto Nacional de Estadística (National Institute for Statistics) (2014) Instituto Nacional de Estadística. Available: http://www.ine.es. Accessed 2014 July 23.
44. Community of Madrid (nd) see “Atlas de la Comunidad de Madrid en el siglo XXI”.
45. Instituto Nacional de Estadística (National Institute for Statistics) (2014) Instituto Nacional de Estadística. Available: http://www.ine.es. Accessed 2014 July 23.
46. Twitter API (nd) section for developers of Twitter Web page. Available: https://dev.twitter.com. Accessed 2014 July 23.
47. Tugores A, Colet P (2013) Big data and urban mobility, Proceeding of the 7th Iberian Grid infrastructure conference.
48. Hastie T, Tibshirani R, Friedman J (2009) The elements of statistical learning (2nd ed.). New York: Springer-Verlag.
49. Roussens P (1967) Silhouettes: A graphical aid to the interpretation and validation of cluster analysis. Journal of Computational and Applied Mathematics 20: 53–65.