Research Article

Study on the Ground Movement in an Open-Pit Mine in the Case of Combined Surface and Underground Mining

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The combined surface and underground mining method is typically used in an open-pit mine for better production and profits. However, the improved scale of mining operations at the combined mining conditions results in even more intensive strata movement and massive ground damages. This paper assesses the progressive development of the characteristics of roof movement with the longwall face advance and its influence on the ground movement at the slope area using physical models. The identification of strata zones at the combined mining conditions is also included. The results show the following: (1) the failure of the competent strong roof creates an inverse arch-shaped rock block structure, which compacts the loose rock fragments in the caved zone; (2) a bed separation occurs above the inverse structure at the top of the disturbed strata configuration and extends upward with the face advance until it approaches the continuous bending zone; (3) more intensive strata movement and ground damages are produced by the large-scale multiseam mining operations, while regular and more distinct strata zones in the disturbed configuration are identified for less intensive single-seam mining; and (4) the intensive and massive underground mining activities increase the slope strata movement at the surface mining side. This research suggests that a less intensive mining activity is preferred in the combined surface and underground mining conditions from the point of view of ground control.

1. Introduction

The surface mining method is mainly used for recovering the reserves at a shallow depth for economic reasons, while the underground mining method is adopted for deep seams. The combined surface and underground mining method is referred to as extracting the reserves using the underground mining method at an open-pit mine [1]. The surface and underground mining operations can be performed either at the same time or separately (simultaneous and nonsimultaneous combined mining operations). The study on the combined surface and underground mining in the case of iron mine has been extensively performed by Bakhtavar. He defined the two major problems in the field of combined mining, which is to find a practicable underground mining method for an open-pit mine for both simultaneous and nonsimultaneous combined mining and to optimize the schedule for the transition from surface mining to underground block cave, particularly in the case of nonsimultaneous mode [2]. For the nonsimultaneous combined mining case, the optimal time for the transition from the surface mining to underground mining was determined from a stochastic mathematical model, and the favourable depth for the transition in an iron mine was determined by considering both geological and economic models [3, 4]. The geotechnical challenges were identified as the induced stress, subsidence, and instability of mine structures which can be mitigated or eliminated by optimization of the crown pillar dimensions [5]. The optimum size of the pillar was calculated from a dimensional analysis to balance the geotechnical problems and economic benefits [6]. In the field of coal mining, the combined mining system can be classified into two categories according to the seam inclination [7]. For steeply inclined seams, the surface mining is operated at the
shallow part, while the underground faces (typically the longwall top coal caving method) are used to extract the coal at a deeper depth. On the other hand, the near-flat seams are worked by both the surface and underground mining operations at approximately the same level. The combined method has been practiced for decades in a number of coal mines in China with further improved production and economic profits. However, one would intuitively expect a more intensive mining-induced ground movement and therefore more damages to the overlying strata and the ground structures especially when the underground longwall faces approach the slopes of the open pit or the dump. This is not only because the mining scale and intensity are significantly increased, but also because it is less likely for the shallow overburden strata in an open-pit mine to form a self-supporting structure. As a result, the combined mining method differs from the other mining technologies in the excavated strata configuration (i.e., the open-pit slope) and the improved ground movement caused by the extensive scale of the surface and underground mining activities. Figure 1 shows the ground movement of the surface and the slope steps captured at Anjialing mine, Shanxi Province. The results showed that multiple times were observed on the ground and the shear movement at the slope strata.

Numerical and physical modelling of the roof caving behaviours has been frequently documented in previous studies for understanding the progressive development of mining-induced fractures and mechanism of strata movement around underground openings. The models have considered the face advance rate on ground movement [8], the extension of caved and fractured zone heights [9], longwall face failure and shield-strata interactions [10–12], and the impact loadings on shields [13]. These models have not considered the combined surface and underground mining method. Sun believes that the damages to the ground are enhanced due to the overlap of the ground movement areas caused by the surface and underground mining activities [14]. Zhu et al. optimized the dimensions of the solid coal pillar (located from one end of the underground longwall face to the slope edge) to improve the stability of the slope [15, 16]. Liu et al. analyzed the influence of the critical distance (the distance from the face position at the slope side perpendicular to the upper slope) on the failure of the slope, based on which they suggested the proper underground mining sequences [17]. However, these models mainly considered the stability and movement of the pit slope; the distribution of the three zones in the overburden for a combined surface and underground is not included.

The three-zone theories of the strata movement in the vertical and horizontal directions are widely accepted by most researchers [18, 19]. The disturbed overlying strata caused by the longwall mining can be identified as three zones in the vertical direction, i.e., the caved zone (Zone I), the fractured zone (Zone II), and the continuous bending zone (Zone III) as shown in Figure 2 [18]. The fractured zone is further divided into the fragmented rock blocks zone, the vertical fracture propagating-through zone, and the horizontally separated zone [18, 19]. The three zones may be reduced to two zones with an absence of the continuous deformation zone at the top in the shallow coal mines in Inner Mongolia of China where the top cover is mainly the unsolidified loose formation [20, 21]. The fractured zone therefore extends to the ground surface as the face advances, leading to an extensive ground movement. The height of the three zones (especially the fractured zone) is closely related to the connectivity of the waste gas and water [22] and can be determined from the empirical equations [23–25], numerical and physical models [26–28], vertical borehole observations [29, 30], and the microseismic monitoring method [31]. Meanwhile, the movement of the overlying strata can also be divided into three zones in the horizontal direction according to the surface subsidence curve. The three horizontal zones are identified as the solid coal support zone (Zone A, where the curve shows the least deformation and the subsidence rate), the separation zone (Zone B, where the bed separation mostly occurs), and the recompressed zone (Zone C, where the loose gob materials in the caved zone and the horizontal bed separation in the fractured zone are recompressed and the surface settlement reaches the maximum).

This paper attempts to study the influence of underground mining on both the overburden migration and the slope stability from physical models. The model configurations are selected from different geological sections of an open-pit mine. The 3 models in the work include different face dimensions: the adjacent-seam mining and multiple-seam mining. The paper has three goals: (1) obtain the progressive development of roof failure and mining-induced strata movement for the combined surface and underground mining conditions; (2) identify the vertical and horizontal zones of the disturbed overburden; and (3) assess the slope behaviours influenced by the underground mining activity.

2. Model Development

2.1. Mine Description. The representative physical model in this study is based on the geological and mining conditions at the Anjialing open-pit mine, Pinghuo, Shanxi Province, where the combined surface and underground mining method is adopted for recovering the 4th and 9th seams at the mine site. The total thickness of No. 4 seam is 8.6–16.8 m and averages at 13.64 m. The immediate roof above No. 4 seam is sandstone with an average thickness of 7.33 m. The weak mudstone and sandy mudstone occasionally occur above the coal seam but cave in upon the face advance. The immediate roof below No. 4 seam is mainly mudstone, below which is the 6.9–16.7 m thick No. 9 seam averaging at 13.8 m. The rock strata between the two near-flat seams are 17.0–57.2 m (average 31.1 m). No. 4 and No. 9 seams were worked at a depth of 170–250 m using the surface mining method. Currently, the coal mine is also recovering the coal seams using the underground longwall top coal caving method. The width of the underground longwall face is 240 m, while the length and the position of the longwall face relative to the slope should be determined based on its influence on the ground movement and the slope stability.
2.2. Similarity Principles and Construction Materials. The physical modelling approach is utilized in this work to reproduce the progressive development of the ground movement and the slope stability of an open-pit mine using the combined surface and underground mining method. One of the most important aspects of the physical modelling is that the physical model must follow a number of similarity principles, according to which the physical features of the model and the prototype case (full-scale case) should be similar in terms of geometry, time, density, and strength. The measurements in the physical model can, therefore, be compared with the real case. The above coefficients are defined as the ratios of corresponding real case parameters over the small-scale physical model and must be kept as constants, which are determined based on the mechanical properties of the modelling materials and the size of the physical modelling rig [8, 12]. In this work, the geometry, time, density, and strength similarity coefficients are determined as 250, 10, 1.47, and 147, respectively.

Proper geomechanical modelling materials are carefully selected to construct the physical model for realistically representing the strata movement. In this work, the construction materials are a mixture of sand, gypsum, and lime with a proper proportion of water. The solid materials are fully mixed before the addition of water to ensure the general homogeneity. The proportions of the physical materials are carefully determined through a trial-and-error process, so that the strata could behave and cave in in a similar way to the real case. The proportions and mechanical properties of the physical materials are given in Tables 1 and 2, respectively.

2.3. Physical Modelling Rig and Model Preparation. The 2D strain plain physical modelling rig used in this research is 500 cm in length, 40 cm in width, and 150 cm in height (see Figure 3). The frame is larger than the traditional ones in order to incorporate the large-scale surface and underground mining activities. Physical materials are first placed in the modelling steel frame and are then compacted to the designed height. The physical model is constructed layer by layer to ensure the overall strength and height of the model. No. 4 and No. 9 seams and the strata shown in Figure 4(a) at the Anjialing open-pit mine are modelled in this study. The right side of the physical model is a slope created by the previous surface mining, while the underground longwall faces are currently operated in the physical models starting from the left side. The physical model has roller boundaries along the left and right side and at the bottom. Figure 3 shows the overall geometry of the physical model. Note that the geometric similarity is 250:1 in this work; therefore, the 500 cm long physical model simulates a total of 1250 m in the real case.

Three models are developed in this research (Models I, II, and III) for representing three geological sections in the studied mine site. In Model I, Face A1 and Face A2 are advanced a total of 200 m in the upper No. 4 seam, followed by a 500 m development of Face B1 in the lower No. 9 seam. A 50 m wide solid coal pillar is maintained between Faces A1 and A2. In Model II, Face B2 and Face B3 are located in the lower No. 9 seam and are worked a total distance of 170 m and 370 m, respectively. A 50 m wide solid coal pillar is left between the two faces. In Model III, Face B4 is mined a total of 500 m in No. 9 seam. The models are developed to study the progressive development of the ground movement, the vertical displacement of the roof strata, and the displacement field of the slope. A 3D digital close-range industrial photogrammetry system is used in this research for providing a
precise, rapid, automatic, and continuous measurement of the strata vertical displacement above the longwall workings. The ground movement in the slope area is also provided by recording the slope deformation field using the digital speckle correlation method. The camera measuring system yields more accurate strata movement results than the traditional electronic theodolite.

3. Results and Analysis

3.1. Model I. Figure 5 plots the progressive development of the ground movement in Model I for recovering both No. 4 and No. 9 seams. Face A₁ in the upper seam was first mined. The face starts at approximately 180 m away from the left boundary of the rig. The roof caves in regularly in the gob area with the face advance, and the caved zone height reaches 10 m above the seam after 120 m of the face advance (Figure 5(a)). With a further 50 m of face development, the more component sandstone roof bends and forms an inverse arch-shaped structure (see the dashed line in Figure 5(b)), beneath which the previously caved loose materials are compacted. A bed separation is also observed above the arch structure at the top of the disturbed overburden, which extends 42.5 m above the seam. Face A₁ advances another 30 m and ceases after a total of 200 m development. During this period, the immediate roof caves in upon the face advance (Figure 5(c)). The main roof beam above the shield is fixed at one end at the solid coal face side and is supported by the inverse arch-shaped structure at the other. As a result, the convergence of the roof should be small and the loading condition of the longwall shield should be better off at this position.
Figure 4: (a) Geological section profile. (b) General stratigraphy for the Anjialing mine.
After completion of Face A1, a 50 m wide coal pillar was left between the previous Face A1 and the adjacent active Face A2. The strata movement for mining Face A2 is shown in Figure 6, which is similar to that of the previous face. The extension of the broken strata increases with the face development. It also reaches 42.5 m after the completion of Face A2 at a total of 200 m face advance (Figure 6(c)).

However, the overall dimension of the disturbed configuration for Face A2 is slightly larger than the previous one, and the gob materials are less compacted by the above inverse arch-shaped strata. The overburden strata above the coal pillar (outlined by the blue dot lines in Figure 6(c)) remain stable and intact. The angle of break (defined as the angle between the vertical line and the edge of stable strata above the pillar) is found at approximately 26° for both panels. The solid coal pillar may yield due to the compression of the stable configuration and the abutment pressures. Mine hazards such as violent coal bursts and extraordinary distortion of the pillar or mine entries may occur.

The influence of multiple-seam mining operations is included in this work by mining Face B1 in the lower seam after the completion of the two faces in the upper seam. In the beginning, the immediate roof collapses in the gob area with the face advance, but the main roof remains intact and the caved height has not reached the previously mined-out gob in the upper seam (Figures 7(a) and 7(b)). In other words, the disturbed strata for Face B1 in the lower seam have not reached the upper gob area; the upper and lower gobs are separated. The loading conditions for the shield and longwall face should be better off at this position since the overburden pressure is partially released through the previous upper gob. After the face has developed 200 m, the main roof caves in as the limit of overhang length is reached (Figure 7(c)). The roof channels between the two coal seams fail completely and the upper gob collapses. The caved zone for the active face extends upward and connects with the upper gob. This may increase the intensity of the roof weighting as well as the shield loading. The channels form an inverse arch-shaped structure compacting the below gob materials and a load-bearing structure supporting the overburden. A huge separation is created at the top of the gob above the structure. The angles of break for both upper and lower faces are similar.

Face B1 advances to the above coal pillar position (Figure 7(d)). The above stable configuration (sitting on the coal pillar between the two upper faces, see Figure 6(c)) transfers the overburden pressures to the active longwall panel and shield. Hence, poor face stability and the tremendous difficulty in advancing the shields might be expected. The load environment in the open face area could return to the previous level only after the face passes the coal pillar area. The face then advances under the upper gob area of Face A2 (Figure 7(e)). The lower gob connects the upper one upon the failure of the roof channel (Figure 7(f)).

Face B1 ceases after 500 m of face development. The final view of the ground movement and the three zones in the horizontal and vertical directions are shown in Figure 8. The zones are different with the typical zone identification shown in Figure 2 because of the extraction of multiple seams. The intensity and extension of ground movement is increased by the multiple-seam mining. A massive ground fracture is observed on the surface above the start position of the longwall face, as well as the shear movement of strata on the slope step. This is consistent with the field observation shown in Figure 1.

Figure 9 shows the vertical displacement of the strata along the face length at different layers above No. 9 seam. Generally, the displacement maximizes at the middle positions of Faces A1 and A2 and reaches a smaller plateau above the solid coal pillar between the two faces. The two-peak shaped curves are formed because of the existence of the stable configuration above the solid coal pillar. It is also noted that the strata at a deeper depth (closer to No. 9 seam) show a larger vertical displacement, with an exception that the roof at 15 m above the seam presents the least vertical displacement and stabilizes at this level (see the blue line). This differs from the other two-peak curves because the roof at 15 m above No. 9 seam stays in the roof channel between the two seams; therefore, the displacement simply represents the strata movement for mining Face B1 rather than for extracting the multiple seams.

The vertical displacement at the slope area is recorded using the digital speckle correlation method. It may not produce the most refined details of the slope displacement field, but the general influence of the underground mining activity to the slope behaviour can be obtained. Figure 10 shows the displacement field after completion of Faces A1,
A2, and B1, respectively. The extraction of Face A1 shows limited impact on the subsidence of the slope (Figure 10(a)), since the finish position of Face A1 is located more than 250 m away from the slope area. Hence, it is inferred that the slope movement is gradually increased with the increase of the scale and intensity of mining activities.

3.2. Model II. In Model II, Faces B2 and B3 in the lower seam are mined with a 50 m coal pillar left between the two panels. The above No. 4 seam remains unmined. The strata

Figure 6: Progressive development of strata movement with advance of Face A2. Face advance distance: (a) 120 m, (b) 170 m, and (c) 200 m.

Figure 7: Progressive development of strata movement with advance of Face B1. Face advance distance: (a) 120 m, (b) 150 m, (c) 200 m, (d) 250 m, (e) 325 m, and (f) 400 m.

Figure 8: Final view of the ground movement at completion of Face B1. I: caved zone; II: fractured zone; and III: continuous bending zone. (A) stable zone; (B) separation zone; and (C) recompacted zone.
movement with the advance of Face B₁ is shown in Figure 11. The caved height extends upward with the face advance (Figures 11(a)–11(c)). The inverse arch-shaped structure compacts the caved loose materials in the gob area (Figure 11(d)). Face B₂ ceases after 170 m of face development.

The adjacent Face B₃ is mined after the completion of the previous Face B₂. The immediate roof caves in upon the face advance. Loose gob materials are regularly placed in the gob area and form the caved zone (Figures 12(a) and 12(b)). With the further face development, the disturbed overburden develops to the fractured zone, and the gob wastes are compacted by the inverse arch-shaped structure (Figures 12(c)–12(e)). The huge bed separation at the top of the disturbed configuration is closed and recreated with the face advance at each face position (see Figures 12(a)–12(e)). However, the recreation of the bed separation terminates after 370 m of face advance when the disturbed strata configuration extends to the continuous bending zone (Figure 12(f)).

Figure 13 provides a final view of the strata movement after completion of Faces B₂ and B₃. The caved zone, fractured zone, and continuous zone in the vertical direction and the stable zone, separation zone, and the recompacted zone in the horizontal direction are also identified. Since Face B₂ only develops a limited distance, no bending zone is observed. By comparison, the bending zone for Face B₃ develops to the ground surface and causes the ground subsidence and surface cracks that are less significant than Model I.

The roof vertical displacement for Model II is given in Figure 14. The maximum displacement is approximately 6 m measuring at the strata at 15 m above No. 9 seam. It decreases with the increase of the distance above the seam and reduces to approximately 3.2 m for the strata at 165 m above the seam. The roof vertical displacement above Face B₂
becomes unnoticeable starting at the strata 40 m above No. 9 seam; therefore, the two-peak curves turn one-peak. It is also observed that, for the vertical displacement above Face B3, the slope rates of the curves at the left side are larger than the right side, corresponding to the more fractured separation zone observed on the left side of Face B3 (see Figure 13).

The contours of the slope vertical displacement after completion of Faces B2 and B3 are shown in Figure 15. The overall vertical displacement is around $-0.5$ to $-1$ m at the cease of Face B2 (Figure 15(a)) and $-1$ to $-1.5$ m for Face B3 (Figure 15(b)). The movement at the slope area is increased as the face approaches the slope [20].

3.3. Model III. In Model III, the only longwall face, Face B4, in the lower seam is mined. The development of strata movement with the face advance is shown in Figure 16. The overall intensity and extension of ground movement is mitigated as compared to the multiple-seam mining in Model I. Figure 16(a) plots the cave of the lower immediate roof extending 5 m above the seam; the cave of the immediate roof occurring at 140 m of face advance is shown in Figure 16(b), extending 12 m above the seam. When the face advances 75 m from the start position, the inverse arch-shaped roof structure and compaction of caved loose gob materials are observed (Figure 16(c)). Extension of disturbed overburden reaches 75 m above the seam, with a notable bed separation at the top of the disturbed configuration. The disturbed strata reach 105 m above the seam after 310 m of the face development (Figure 16(d)). The strata then extend to the ground surface at a further 60 m of face advance, where the bed separation is closed (Figure 16(e)). The dimension of the broken strata grows gradually with face development, but the general configurations look similar (Figures 16(f) and 16(g)). Face B4 ceases after 500 m of face advance.

Figure 17 identifies the caved zone, the fractured zone, and the bending zone in the vertical direction as well as the stable zone supported by the solid coal, the bed separation zone, and recompacted zone in the horizontal direction after the completion of Face B4. Since no pillar is maintained between panels, no superposition of the zones occurs. Therefore, the identified zones in the vertical and horizontal directions are more distinct and are similar to the typical zones shown in Figure 2. It also shows that the ground subsidence and cracks seem less distinct than Models I and II. The angle of break is about 30°, which is similar to previous models.
The vertical displacement of the strata at different distance above No. 9 seam is shown in Figure 18. The strata displacement starts to increase at the junction between the stable zone and separation zone. It reaches the maximum in the recompacted zone. Generally, the overburden strata closer to No. 9 seam show a larger displacement. At 15 m above the seam, the largest vertical displacement is about 3.8 m, compared with only 2 m of vertical displacement at 165 m above the seam.

The comparison of roof vertical displacement for different models is given in Table 3. Due to the bed separation in the caved and fractured zones, it is more proper to compare the displacement at 165 m above the seam, which represents the ground movement in the continuous bending zone. Model I shows the largest strata displacement mainly due to the intensive multiseam mining activity, followed by Models II and III in the descending order. The shallower depth of cover for Model II might be responsible for the relative larger displacement than Model III.

The slope vertical displacement field after completion of Face B4 is shown in Figure 19. The overall vertical displacement is around 0 to −2 m. As compared to Models I and
II, the slope movement is slightly mitigated. The ground movement at the slope area may depend on the intensity of mining activities and the mining positions relative to the

Figure 16: Progressive development of strata movement with advance of Face B₄. Face advance distance: (a) 70 m, (b) 140 m, (c) 220 m, (d) 310 m, (e) 370 m, (f) 470 m, and (g) 500 m.

Figure 17: Final view of the ground movement at completion of Face B₄. I: caved zone; II: fractured zone; and III: continuous bending zone. (A) stable zone; (B) separation zone; and (C) recompacted zone.

Table 3: Comparison of roof vertical displacement at 15 m and 165 m above No. 9 seam.

| Strata vertical displacement | Model I (m) | Model II (m) | Model III (m) |
|-----------------------------|-------------|--------------|---------------|
| 15 m above No. 9 seam       | 10          | 6            | 3.8           |
| 165 m above No. 9 seam      | 7           | 3.2          | 2             |

Figure 18: Strata vertical displacement after completion of Face B₄.

Figure 19: Slope vertical displacement contour after completion of Face B₄.
mine slope. The slope movement is increased with the increase of mining intensity and the approach of longwall face to the slope.

4. Discussion and Conclusions

With the development of the dimensions of the open pit, the coal mine starts to adopt the underground longwall mining method for recovering the coal seam to improve the production and profits. However, the ground movement and surface subsidence may also be increased due to the intensive and large-scale combined surface and underground mining activities. In this paper, the ground movement of the combined surface and underground mining of an open-pit mine is reproduced on a large-size physical modelling rig. Three physical models are developed to assess the roof vertical displacement, and the zone identification along the horizontal and vertical directions. The influence of the underground mining on the ground movement at the slope area is also included. Important findings of this study are listed below.

1. Faces A₁ and A₂ in the upper seam and Face B₁ in the lower seam are included in Model I. Faces A₁ and A₂ are first mined, followed by the extraction of Face B₁. An inverse arch-shaped roof block structure is created upon the failure of the competent strong roof. The structure compacts the loose gob materials in the caved zone but leaves a bed separation at the top of the disturbed configuration. During the extraction of Face B₁, the caved and fractured zones for the lower seam extend and connect with the upper ones, leading to the massive collapse of the overburden strata. Massive ground cracks and shear movement on the slope step are created by the large-scale multiseam mining activities. The maximum roof vertical displacement in the continuous bending zone reaches 6 m.

2. Faces B₁ and B₂ in the lower seam are mined in Model II. A 50 m coal pillar is maintained between the two faces. The ground movement is much mitigated as compared to Model I. The bed separation above the inverse arch-shaped structure extends upward with the face advance and is closed when it reaches the continuous bending zone. Only the caved and fractured zones are observed above Face B₁ due to the limited distance of face advance, while the continuous bending zone is found above Face B₂. The ground crack is also observed on the surface but is significantly smaller than the massive crack caused by the intensive multiseam mining. The vertical displacement of the strata in the continuous zone (at 165 m above No. 9 seam) is about 3.2 m.

3. Face B₃ in the lower seam advances a total of 500 m in Model III. This face is the only longwall face in the model; therefore, the three zones in the vertical and horizontal directions are clearly identified and no superposition of the zones is observed. The angle of break after completion of the face is approximately 30°, similar to the rest of the faces. The strata in the continuous bending zone displace 2 m in the vertical direction.

4. The ground movement in the slope area is mostly affected by the underground mining in Model I, followed by Models II and III in the descending order. The extent of slope movement increases with not only the intensity and scale of the mining activity, but also as the longwall face approaches the slope.

Data Availability

The data used to support the findings of this study are included within the article.

Conflicts of Interest

The authors declare that there are no conflicts of interest regarding the publication of this paper.

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