Data Article

Missing data estimation in extreme rainfall indices for the Metropolitan area of Cali - Colombia: An approach based on artificial neural networks

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A B S T R A C T

Changes observed in the current climate and projected for the future significantly concern researchers, decision-makers, and the general public. Climate indices of extreme rainfall events are a trend assessment tool to detect climate variability and change signals, which have an average reliability at least in the short term and given climatic inertia. This paper shows 12 climate indices of extreme rainfall events for annual and seasonal scales for 12 climate stations between 1969 to 2019 in the Metropolitan area of Cali (southwestern Colombia). The construction of the indices starts from daily rainfall time series, which although have between 0.5% and

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5.4% of missing data, can affect the estimation of the indices. Here, we propose a methodology to complete missing data of the extreme event indices that model the peaks in the time series. This methodology uses an artificial neural network approach known as Non-Linear Principal Component Analysis (NLPCA). The approach reconstructs the time series by modulating the extreme values of the indices, a fundamental feature when evaluating extreme rainfall events in a region. The accuracy in the indices estimation shows values close to 1 in the Pearson’s Correlation Coefficient and in the Bi-weighting Correlation. Moreover, values close to 0 in the percent bias and RMSE-observations standard deviation ratio. The database provided here is an essential input in future evaluation studies of extreme rainfall events in the Metropolitan area of Cali, the third most crucial urban conglomerate in Colombia with more than 3.9 million inhabitants.

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### Specifications Table

| Subject                                      | Environmental Science – Climatology               |
|----------------------------------------------|--------------------------------------------------|
| Specific subject area                       | Missing data estimation in extreme annual and seasonal rainfall indices using an artificial neural network approach. |
| Type of data                                 | Figures and tables                               |
| How the data were acquired                   | Daily rainfall data were obtained following the procedures established by the Corporación Autónoma Regional del Valle del Cauca (CVC) and the Instituto de Hidrología, Meteorología y Estudios Ambientales (IDEAM) of Colombia. |
| Data format                                  | Analyzed data Spreadsheet                        |
| Description of data collection              | The climate extreme indices were estimated using the ClimInd package, and the indicators are based on daily rainfall (RR) information of surface data. Annual and seasonal extreme rainfall indices were PRCP�OT, RX1day, RX5day, d95p, CWD, CDD, R1mm, R3mm, R10mm, R20mm, and SDII. Missing data estimation in extreme annual and seasonal rainfall indices using an auto-associative neural network known as the Non-Linear Principal Component Analysis approach. |
| Data source location                         | Metropolitan Area of Cali, Valle del Cauca–Colombia. |
| Data accessibility                          | The daily rainfall dataset is accessible on the CVC: [https://ecopedia.cvc.gov.co/portal-hidroclimatologico.html](https://ecopedia.cvc.gov.co/portal-hidroclimatologico.html) and IDEAM: [http://dhime.ideam.gov.co/atencionciudadano/](http://dhime.ideam.gov.co/atencionciudadano/). Extreme rainfall index series are available in this article. |

### Value of the Data

- Data from this article can be used to (a) visualize the relevance of climate risk management studies, (b) improve trend analyses of extreme rainfall events, (c) analyze changes in extreme rainfall indices related to climate variability and change, (d) identify homogeneous climatic regions, and (e) increase the reliability of forecasting in extreme rainfall events.
- The datasets of extreme rainfall indices assess the intensity, frequency, and duration of extreme weather events.
- This dataset can be a proxy for hydrometeorological hazards such as droughts, floods, and heavy rains in the analyzed region.
Table 1
Descriptive statistical analysis of the daily rainfall data in the Metropolitan Area of Cali (1969–2019).

| ID | Station          | Rainfall mean (mm.year⁻¹) | Annual rainfall standard deviation (mm) | Daily Average (mm) | Daily rainfall standard deviation (mm) |
|----|------------------|---------------------------|----------------------------------------|--------------------|----------------------------------------|
| 1  | Vjies            | 890.9                     | 258.8                                  | 2.5                | 6.7                                    |
| 2  | Ing. Manuelita   | 1142.1                    | 346.2                                  | 3.1                | 8.0                                    |
| 3  | Colegio Sj Bosco | 1157.2                    | 455.1                                  | 3.3                | 8.2                                    |
| 4  | Univalle         | 1397.4                    | 211.3                                  | 4.0                | 9.6                                    |
| 5  | Los Cristales    | 1757.7                    | 225.6                                  | 4.9                | 11.2                                   |
| 6  | Las Brisas       | 1966.8                    | 432.5                                  | 5.6                | 12.5                                   |
| 7  | Brasilia         | 1470.9                    | 218.7                                  | 4.1                | 8.5                                    |
| 8  | La Teresita      | 1755.9                    | 380.1                                  | 4.9                | 9.3                                    |
| 9  | La Fonda         | 1948.7                    | 542.0                                  | 5.4                | 12.2                                   |
| 10 | El Topacio       | 2803.2                    | 395.0                                  | 7.7                | 14.1                                   |
| 11 | Florida          | 1544.5                    | 388.1                                  | 4.3                | 11.0                                   |
| 12 | La Balsa         | 2125.8                    | 388.9                                  | 5.9                | 12.2                                   |

- The new dataset is useful for institutions, researchers, and experts involved in climate risk management, water resource management, and other fields related to climate variability and change.

1. Data Description

This paper reports the time series of extreme rainfall indices for the Metropolitan area of Cali in southwestern Colombia – South America (Fig. 1) between 1969 to 2019. Daily rainfall time series from 12 stations were used to construct the extreme rainfall indices. The stations are presented in Fig. 1 and the statistical description of the rainfall data series is given in Table 1. The

![Fig. 1. Localization of the rainfall gauge stations in Metropolitan Area of Cali, Valle del Cauca–Colombia.](image-url)
Table 2
Climatic indices based on the daily rainfall.

| Label      | Index name                      | Description                                                                 | Units   |
|------------|---------------------------------|-----------------------------------------------------------------------------|---------|
| PRCPTOT    | Total wet-day rainfall          | Rainfall amount on days with RR \( \geq 1 \) mm                            | mm      |
| RX1day     | The highest amount of daily rainfall | The maximum consecutive 1-day rainfall                                      | mm      |
| RX5day     | The maximum consecutive 5-day rainfall | The maximum consecutive 5-day rainfall                                      | mm      |
| d95p       | Very wet days                   | Days with rainfall > 95p                                                    | days    |
| CDD        | Consecutive wet days            | The maximum length of consecutive wet days (RR \( \geq 1 \))                | days    |
| DryDays    | Dry Days                        | Number of days with less than 1 mm                                          | days    |
| R1 mm      | Wet days 1 mm                   | Annual count of wet days                                                    | days    |
| R3 mm      | Wet days 3 mm                   | Annual count of days when RR \( \geq 3 \) mm                               | days    |
| R10 mm     | Wet days 10 mm                  | Annual count of days when RR \( \geq 10 \) mm                              | days    |
| R20 mm     | Wet days 20 mm                  | Annual count of days when RR \( \geq 20 \) mm                             | days    |
| SDII       | Simple rainfall intensity index  | Sum of rainfall in wet days (days with >1 mm of rainfall), and dividing that by the number of wet days in the period | mm.day\(^{-1}\) |

*RR is the daily rainfall

Table 3
Percentage of missing data for daily rainfall data and time scales of extreme rainfall indices.

| ID | Station             | Missing data (%) |
|----|---------------------|------------------|
|    |                     | Daily rainfall   | Annual indices | DJF indices | MAM indices | JJA indices | SON indices |
| 1  | Vijes               | 3.54             | 13.73          | 13.73       | 1.96        | 5.88        | 11.76       |
| 2  | Ing. Manuelita      | 2.46             | 7.84           | 5.88        | 5.88        | 3.92        | 1.96        |
| 3  | Colegio SJ Bosco    | 3.00             | 21.57          | 39.22       | 33.33       | 27.45       | 41.18       |
| 4  | Univalle            | 5.38             | 27.45          | 35.29       | 27.45       | 39.22       | 52.94       |
| 5  | Los Cristales       | 1.43             | 15.69          | 7.84        | 7.84        | 11.76       | 9.80        |
| 6  | Las Brisas          | 3.54             | 17.65          | 15.69       | 3.92        | 11.76       | 11.76       |
| 7  | Brasilia            | 0.82             | 5.88           | 9.80        | 5.88        | 15.69       | 7.84        |
| 8  | La Teresita         | 3.95             | 23.53          | 21.57       | 17.65       | 21.57       | 21.57       |
| 9  | La Fonda            | 1.33             | 13.73          | 9.80        | 0.00        | 3.92        | 5.88        |
| 10 | El Topacio          | 0.53             | 1.96           | 3.92        | 11.76       | 15.69       | 5.88        |
| 11 | Florida             | 1.04             | 7.84           | 1.96        | 1.96        | 1.96        | 9.80        |
| 12 | La Balsa            | 0.74             | 5.88           | 7.84        | 1.96        | 0.00        | 5.88        |

The total annual rainfall for the overall period is between 890.9 and 2803.2 mm, and the standard deviation varies between 211.3 and 542 mm. The mean daily rainfall amounts ranges from 2.5 and 7.7 mm day\(^{-1}\), with a standard deviation between 6.7 and 14.1 mm day\(^{-1}\) (See Table 1).

Twelve rainfall extreme indices were selected, which monitor rainfall intensity (5 indices), frequency (5 indices), and duration (2 indices). The description of the climate indices based on daily rainfall used is presented in Table 2.

Rainfall stations up to 6% of missing data in the considered period were selected. The daily rainfall series contained missing data, consequently the extreme rainfall index series is also compromised. Due to the criteria adopted in its calculations, the percentage of missing data of the extreme rainfall indices is typically higher than the daily data percentage. Zhang et al. [1] specify that a monthly index is not calculated if more than three daily data are missing in a month, and an annual index is not calculated if more than 15 spread daily data or a month are missing in
Fig. 2. Flowchart of the NLPCA. \( x_0 \) is the input layer (Extreme rainfall indices), \( y_m \) is the bottleneck layer of the NLPCA model, and \( \tilde{x}_n \) is the output layer (Extreme rainfall indices reconstructed).

Table 4

| Name                                      | Equation                                                                 | Units | Perfect Score |
|-------------------------------------------|--------------------------------------------------------------------------|-------|---------------|
| Pearson’s correlation coefficient (CC)    | \( CC = \frac{\sum_{i=1}^{N_c} (Y_i - \bar{Y})(X_i - \bar{X})}{\sqrt{\sum_{i=1}^{N_c} (Y_i - \bar{Y})^2 \sum_{i=1}^{N_c} (X_i - \bar{X})^2}} \) | -     | 1.0           |
| Biweight midcorrelation (Bicor)            | \( \text{Bicor} = \frac{\sum_{i=1}^{N_c} (Y_i - \bar{Y})(X_i - \bar{X})}{\sqrt{\sum_{i=1}^{N_c} (Y_i - \bar{Y})^2 \sum_{i=1}^{N_c} (X_i - \bar{X})^2}} \) | -     | 1.0           |
| Percent bias (Pbias)                      | \( \text{Pbias} = \frac{\sum_{i=1}^{N_c} (Y_i - \bar{Y})^2 \times 100}{\sum_{i=1}^{N_c} (Y_i)^2} \) | %     | 0.0           |
| RMSE- observations standard deviation ratio (RSR) | \( \text{RSR} = \frac{\sum_{i=1}^{N_c} (Y_i - \bar{Y})^2}{\sum_{i=1}^{N_c} (Y_i)^2} \) | -     | 0.0           |

where \( Y_i = \) estimated index during \( i \) period, \( Y_0 = \) observed index, \( N \) is the number of observations, \( \xi xx \) is the biweight midvariance of \( xx \), \( \xi yy \) is the biweight midvariance of \( yy \), and \( \xi xy \) is the biweight midcovariance of \( xx \) and \( yy \).

a year. Table 3 shows the percentage of missing data for the daily precipitation time series and the percentage of missing data for the extreme rainfall indices for annual and seasonal scales.

The missing data of the climate indices were filled using the complete Non-Linear Principal Component Analysis (NLPCA) topology, where the decoder is used after the bottleneck, i.e., the inverse NLPCA, which takes the principal components to recover the original information. Fig. 2 shows the flow chart of the methodology.

Fig. 3 shows the heat map constructed with R v.4.1.2 using ggplot package that representing the performance metrics of extreme precipitation indices at annual and seasonal scales. The assessed through the Pearson’s correlation coefficient (CC), Bi-weighting correlation (Bicor), percent bias (Pbias), and RMSE-observations standard deviation ratio (RSR) was estimated. The rows represent the extreme rainfall indices, and the columns represent the stations grouped by the time scales studied. The performance in the estimation of extreme rainfall indices is highlighted with CC and Bicor (Pbias and RSR) values close to 1 (0) in the all-time series, except for CWD and PRCPPTOT during December to February (DJF) and June to August (JJA), respectively. The equations for CC, Bicor, Pbias and RSR are shown in Table 4.

The data of the observed and estimated extreme rainfall indices are shown in Figs. 4–7. Here, the annual series for two intensity indices (the highest amount of daily rainfall - RX1day, and very wet days - d95p), a frequency index (number of days for rainfall \( >= 20 \text{ mm–R20 mm} \)), and a duration index (consecutive dry days - CDD) were presented. Four stations with a high
Fig. 3. Statistics of missing data estimation error obtained for annual and seasonal extreme rainfall indices from 1969 to 2019 over twelve rainfall stations (Fig. 1). Furthermore, for Pbias and RSR dark (light) colors indicate better (worse) statistical estimation.

percentage of missing data in extreme rainfall indices at the annual scale were plotted: Uni-valle (27%), La Teresita (24%), Col. SJ Bosco (22%), and Los Cristales (16%) (see Table 3). All the time series and graphs for the station’s rainfall gauges at the annual/seasonal scales indices are available in the Appendix.

2. Experimental Design, Materials and Methods

2.1. Study area description

The Metropolitan area of Cali (MAC) is located in southwestern Colombia, dynamically structured as a territorial and functional unit based on a physical environment. The MAC is the third-largest Metropolitan area in the country, with an estimated population of 3.9 million inhabitants in 2018 [2,3]. The MAC comprises Cali, Candelaria, Jamundí, Palmira, Florida, Pradera, and Yumbo, covering 3580 km² in the geographic valley of the Cauca River, the most important basin in the country. The MAC’s geomorphological, geological, and hydroclimatological characteristics promote hydrological hazards (e.g., floods and droughts), negatively affecting its economic and social development [4–6]. Therefore, the socio-economics of the region is affected, includ-
**Fig. 4.** Annual observed time series of the highest of daily rainfall – RX1day index versus annual estimates for rainfall stations (a) Univalle, (b) La Teresita, (c) Col. SJ Bosco, and (d) Los Cristales.

**Fig. 5.** Annual observed time series of very wet days – d95p index versus annual estimates for rainfall stations a) Univalle, b) La Teresita, c) Col. SJ Bosco, and d) Los Cristales.
Fig. 6. Annual observed time series of the number of days for rainfall $\geq 20$ mm–R20 mm index versus annual estimates for rainfall stations a) Univalle, b) La Teresita, c) Col. SJ Bosco, and d) Los Cristales.

Fig. 7. Annual observed time series of consecutive dry days – CDD index versus annual estimates for rainfall stations a) Univalle, b) La Teresita, c) Col. SJ Bosco, and d) Los Cristales.
ing losses in extensive territories dedicated to agriculture and livestock, urban and rural areas, partial or total destruction of infrastructure, and energy deficits [5,7,8].

2.2. Material and methods

2.2.1. Rainfall indexes

The climate rainfall extreme indices were calculated using the ClimInd package (Available in http://etccdi.pacificclimate.org/software.shtml) [1]. The indicators are based on daily rainfall (RR) information (Table 2) of surface data (Table 1). Finally, 12 climate indices were selected related to rainfall extremes’ intensity, frequency, and duration. The indexes are determined on the yearly and seasonal scale of each rainfall station.

2.2.2. Missing data estimation

Considering that some stations exhibited more than 3 or 15 missing days at seasonal and annual scales, respectively. The auto-associative artificial neural network approach called NLPCA to estimate missing data in the time series of extreme rainfall indices were used. The methodology applied for the missing data estimation is based on the decoder, the second phase of the NLPCA, known as inverse NLPCA, a non-linear generalization of the standard Principal Component Analysis when they want to go back to the original representation. This algorithm was established by Scholz et al. [9,10], and was used to estimate missing data in the field of hydro-climatology by Miró et al. [11] and Canchala et al. [12].

The inverse NLPCA uses the reconstruction function $\Phi_{gen}: y \rightarrow \tilde{x}$, performed by a feed-forward network. Eq. (1) shown the output $\tilde{x}$ is dependent upon the input $X$ and the ANN weights $w\in W_3, W_4$.

$$\tilde{x} = \Phi_{gen}(w, y) = W_4g(W_3y)$$ (1)

where the goal of the $\Phi_{gen}$ is to estimate a dataset $\tilde{x}$ approximate to the target data $x$ by minimizing the squared error $\|x - \tilde{x}\|^2$. More details about this technique are available in Scholz et al. [10,11], and the NLPCA toolbox used in this study is available at http://www.nlPCA.org/matlab.html.

The missing data of the annual and seasonal extreme rainfall indices were obtained using the extreme rainfall indices described in Table 3 as the inputs and a [12,11,12] network topology (see Fig. 2).

Ethics Statements

The authors agree that there are no ethics statements to be made.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

CRediT Author Statement

Camilo Ocampo-Marulanda: Conceptualization, Methodology, Software, Data curation, Writing – original draft, Visualization, Investigation; Wilmar L. Cerón: Conceptualization, Methodology, Software, Writing – original draft, Writing – review & editing, Visualization, Investigation; Alvaro Avila-Diaz: Conceptualization, Methodology, Software, Data curation, Writing – original draft; Teresita Canchala: Supervision, Writing – original draft; Wilfredo Alfonso-Morales: Supervision, Writing – original draft, Writing – review & editing; Mary T. Kayano: Supervision, Writing – review & editing; Roger R. Torres: Supervision, Writing – review & editing.
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Supplementary Materials

Supplementary material associated with this article can be found in the online version at doi:10.1016/j.dib.2021.107592.

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