Cryogenic characterization of a LiAlO$_2$ crystal and new results on spin-dependent dark matter interactions with ordinary matter

CRESST Collaboration

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Abstract In this work, a first cryogenic characterization of a scintillating LiAlO$_2$ single crystal is presented. The results achieved show that this material holds great potential as a target for direct dark matter search experiments. Three different detector modules obtained from one crystal grown at the Leibniz-Institut für Kristallzüchtung (IKZ) have been tested to study different properties at cryogenic temperatures. Firstly, two 2.8 g twin crystals were used to build different detector modules which were operated in an above-ground laboratory at the Max Planck Institute for Physics (MPP) in Munich, Germany. The first detector module was used to study the scintillation properties of LiAlO$_2$ at cryogenic temperatures. The second achieved an energy threshold of $(213.02 \pm 1.48)\text{ eV}$ which allows setting a competitive limit on the spin-dependent dark matter particle-proton scattering cross section for dark matter particle masses between $350 \text{ MeV/c}^2$ and $1.50 \text{ GeV/c}^2$. Secondly, a detector module with a 373 g LiAlO$_2$ crystal as the main absorber was tested in an underground facility at the Laboratori Nazionali del Gran Sasso (LNGS): from this measurement it was possible to determine the radiopurity of the crystal and study the feasibility of using this material as a neutron flux monitor for low-background experiments.

Keywords Dark matter · Cryogenics · Spin-dependent · Lithium · Neutrons

1 Introduction

In the past few decades, great effort has been devoted to the investigation of dark matter [1]. One path which could lead to the identification of this elusive particle(s) is that of direct detection experiments. The goal of most experiments in this class is to detect interactions of a dark matter
particle with nuclei of a target material [2]. The CRESST (Cryogenic Rare Event Search with Superconducting Thermometers) experiment, like most other direct searches, has primarily focused on probing spin-independent dark matter-nucleus interactions [3]. CRESST [4] is currently operating CaWO4 and Al2O3 crystals at cryogenic temperatures in the LNGS underground laboratory located below the Gran Sasso massif in Italy. One advantage of this experiment is that the technology is not necessarily tied to the target employed; it is relatively easy to change the target crystal and thereby take advantage of the properties of different target nuclei.

In 2019, the CRESST Collaboration published the first results obtained with a lithium-based crystal operated in an above-ground laboratory [5], showing great potential for dark matter searches using lithium-containing crystals. Lithium is an attractive material because it is the lightest element that can be tested with the CRESST technology, which consists of a scintillating crystal equipped with a tungsten based Transition Edge Sensor (TES) operated at cryogenic temperatures. Since CRESST is heavily oriented towards the search for dark matter particles with sub-GeV mass, the adoption of crystals containing light elements can boost this exploration due to the favorable kinematics. Furthermore, lithium is one of the best elements to investigate spin-dependent interactions, being mainly constituted of 7Li (92.41% natural abundance [6]), which has $J_N = 3/2$ and $\langle S_p \rangle = 0.497$ [7]. We do not investigate spin-dependent interactions with 6Li because of the current lack of $\langle S_{p/n} \rangle$ values in the available literature.

Another appealing property of these crystals is the possibility to detect the $6\text{Li}(n,\alpha)^3\text{H}$ reaction:

$$^6\text{Li} + n \rightarrow \alpha + ^3\text{H} + 4.78 \text{ MeV}. \quad (1)$$

In fact, one of the most challenging sources of background for a direct dark matter search experiment are neutrons which, like dark matter particles, induce nuclear recoils. Through the detection of the above reaction, which shows a distinctive signature in a scintillating bolometer [8,9], it is viable to precisely measure the neutron flux inside the experimental setup and, with the support of Monte Carlo simulations, it might be possible to reconstruct the energy spectrum of the neutrons.

There are many crystals containing lithium that can be employed, such as Li2MoO4 [8,10], Li2Mg2(MoO4)2 [11], Li2WO4 [12], and LiF [13,14]. Amongst these, a crystal with promising properties is LiAlO2. First, the CRESST technology for the direct deposition of a TES on the crystal surface can be applied. Second, LiAlO2 is a scintillator at room temperature and shows a light emission with a 340 nm peak [15] at which the CRESST light detectors have a high absorption [16]. Finally, LiAlO2 also contains $^{27}\text{Al}$ (100.0% natural abundance [6]), another interesting element to study spin-dependent interactions, with $J_N = 5/2$ and $\langle S_p \rangle = 0.343$ [17]. The crystal used to build the detector modules operated in this work was produced at the Leibniz-Institut für Kristallzüchtung (IKZ) in Berlin and Sect. 2 is dedicated to a summary of the growth procedure. The following sections respectively detail the experimental setup, the data collected for the cryogenic characterization, the neutron and radiopurity measurements, and the dark matter results.

## 2 Crystal growth

All the detector modules used in this work are based on LiAlO2 targets obtained from one single crystal grown at IKZ. The original crystal had a 5 cm diameter and was produced using the Czochralski technique [18]. The primary challenge for the growth of this kind of material stems from its high melting temperature of 1780 °C, which entails a strong Li2O evaporation. Li2O evaporates not only from the melt, but also from the growing crystal: in unfavorable thermal conditions, this evaporation is so strong that an Li-free shell of $\alpha$-Al2O3, a few millimeters thick, can form around the LiAlO2 crystal. To avoid crystal decomposition which would arise from this effect, the axial thermal gradient in the setup must be kept as steep as possible. However, a steep temperature gradient implies an increased superheating of the melt associated with an intensified Li2O evaporation from the melt itself: this shifts the melt composition from the desired one towards an Al2O3-rich melt. Because of non-identical melt and crystal compositions, the crystallization with Al2O3-rich melt involves solute segregation. To a certain extent, this results in the degradation of the grown crystals, in the form of a non-uniform macro distribution of the constituting elements and/or micro-inhomogeneities like second-phase inclusions, mainly LiAl5O8, due to reduced interface stability. There is no perfect set of growth conditions and parameters which can avoid all the effects of Li2O evaporation: a practical solution will necessitate a compromise among crystal perfection, crystal size, and cost of the process.

The crystal used in this work was grown inside a cylindrical iridium crucible of 100 mm diameter in an argon protective atmosphere. The raw materials used for the crystal production are Li2CO3 and Al2O3 compounds with a 4N/5N purity. Special attention was paid to the preparation of the raw material in order to prevent Li2O losses before the crystal growth: these materials were weighed and mixed in a stoichiometric ratio and calcinated at temperatures between 700 °C and 750 °C in platinum crucibles. The temperature and duration for this preparation was deduced from thermogravimetric measurements of the starting materials [19].

During the crystal growth, the axial temperature gradient was increased step-wise by changing the thermal insulation, until the opaque Al2O3 shell disappeared entirely and a shiny transparent crystal was obtained. This was achieved by apply-
ing a pulling rate of 1.5 mm/h when growing along the (100) direction, together with a crystal rotation between 10 and 25 rpm to improve the melt mixing. A more detailed description of the growth procedure, crystal defects, and tuning of the parameters can be found in [20].

3 Experimental setup at Max Planck Institute

Two \((20 \times 10 \times 5) \text{ mm}^3\) crystals with a mass of 2.8 g each were cut from the LiAlO\(_2\) single crystal produced at IKZ, and were used to assemble two different detector modules.

The first crystal was used to assemble module A, a detector module (see Fig. 1) designed to characterize LiAlO\(_2\) at cryogenic temperatures. In this case, the crystal was instrumented with a Neutron Transmutation Doped (NTD) germanium thermistor [21] glued\(^1\) to one surface. The crystal was held in position inside a copper frame by two strings of PTFE tape. Electrical and thermal connections to the NTD were provided via 25 \(\mu\text{m}\) diameter gold bond wires. The temperature variation of the NTD was obtained by measuring the resistance of the thermistor. To do so, a constant bias current was sent through the NTD and the voltage drop of the sensor was measured with a commercial differential voltage amplifier.\(^2\) A CRESST-III light detector (LD) [16] was facing the crystal, held in position by two CuNi clamps; this LD was made of a sapphire plate with a 1 \(\mu\text{m}\) silicon layer epitaxially grown on one face (Silicon-on-Sapphire) with a TES as thermal sensor deposited on the silicon side. The readout of the light detector is obtained with a commercial SQUID system,\(^3\) combined with a CRESST-like detector control system [22]. An \(^{55}\text{Fe}\) X-ray source with an activity of \(\sim 0.05\) Bq was placed at a distance of \(\sim 0.5 \text{ cm}\) from the light detector to calibrate its energy response. The TES on the LD had a critical temperature \(T_{C,LD} = 22 \text{ mK}\).

The second crystal constituted the main absorber of module B (Fig. 2), a detector designed to reach a low energy threshold (< 1 keV). The crystal was held in position inside a copper frame by two CuNi clamps. On one face of the crystal, a TES with a design similar to that of the light detector was deposited. The TES is constituted by a thin strip of tungsten with two large aluminum pads partially overlapping the tungsten layer. The aluminum pads serve two different purposes, as phonon collectors and as bond pads. The bond pads are connected via a pair of 25 \(\mu\text{m}\) aluminum bond wires through which the bias current is injected. The tungsten film is also connected by a long and thin strip of gold to a thicker gold bond pad on which a 25 \(\mu\text{m}\) gold wire is bonded. The gold strip serves as a weak thermal link between the sensor and the heat bath at \(\sim 10 \text{ mK}\). On the same surface, but separated from the TES, there is an evaporated heater made of a thin strip of gold with two aluminum pads deposited on top. These pads are bonded with a pair of 25 \(\mu\text{m}\) aluminum bond

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\(^1\) GP 12 Allzweck-Epoxidkleber, Gößl + Pfaff.
\(^2\) Stanford Research System—SR560 Low-noise voltage preamplifier.
\(^3\) Applied Physics System model 581 DC SQUID.
Fig. 3 Measurement of resistance versus temperature with 3 different bias currents applied to the TES on module B. At \(~\sim 42.5\) mK there is a transition between a superconducting response and a normal conducting response (Critical Temperature $T_C$) measured with a $4 \mu A$ bias current. The $T_C$ has a slight dependence on the bias current applied to the TES caused by the electrothermal feedback wires through which a tunable current is injected to maintain the TES at the desired temperature. The heater is also used to inject heater pulses to monitor the detector response over time and for calibration purposes.

This TES had a critical temperature $T_C^B \simeq 42.5\) mK (Fig. 3) when operated with a $4 \mu A$ bias current. $T_C^B$ is rather high compared to usual transition temperatures of CRESST TESs ($\sim 15\) mK); this can negatively affect the performance of the calorimeter, resulting in a higher energy threshold.

The two modules have been operated together inside a Leiden Cryogenics dilution refrigerator at the Max Planck Institute for Physics in Munich, Germany. The dilution refrigerator is located in an above-ground laboratory without shielding against environmental and cosmic radiation. The modules have been mechanically and thermally connected to the coldest point of the dilution refrigerator ($\sim 10\) mK).

4 First cryogenic characterization of LiAlO$_2$

Since there is no literature available on the cryogenic performance of LiAlO$_2$, the starting point was to study its basic properties. This was done using module A, which allowed an initial overview on scintillation, light yield (LY), and Quenching Factors (QFs)$^4$ [23–25] for different particle interactions inside the crystal.

The energy calibration of the light detector was performed using the peaks originating from the $^{55}$Fe source (Fig. 4). After calibration, the baseline resolution of the light detector

\[ \sigma_{LD, baseline} = (26.64 \pm 1.20)\) eV, \]

while the resolution at $5.895\) keV is $\sigma_{Fe} = (123.9 \pm 4.1)\) eV.

During the operation of module A, an AmBe neutron source was installed at a distance of $\sim 50\) cm from the center of the dilution refrigerator. For the energy calibration of the NTD the neutron capture peak appearing at $4780\) keV (Eq. 1) was used, where the energy resolution is $\sigma_{capture} = (19.96 \pm 0.72)\) keV.

In Fig. 5, the energy measured in the light channel is plotted versus the energy measured in the phonon channel for each event registered by the detector during 9.44 h of effec-
tive measuring time in the presence of the AmBe neutron source. Three main different families of events are easily distinguishable. Gamma and beta particles interacting in the LiAlO$_2$ form one band starting from zero energy and with a light yield of $(1.180 \pm 0.103)$ keV/MeV, where the LY is defined as:

$$\text{LY} = \frac{\text{Energy}_{\text{LD}}}{\text{Energy}_{\text{NTD}}}$$

(2)

Neutrons scattering within the crystal exhibit a band starting from zero energy as well, but with a much reduced light yield $(0.284 \pm 0.056)$ keV/MeV, resulting in a Quenching Factor for neutrons equal to 0.241. At high energies and with a light yield of $\sim 0.75$ keV/MeV (or $(3.438 \pm 0.227)$ keV at 4.78 MeV), in between the $\beta/\gamma$ band and the neutron band, the neutron capture by $^6\text{Li}$ appears. Assuming a linear light emission up to this energy, the QF for the neutron capture is 0.599.

The separation between the $\beta/\gamma$ band and the neutron band starts to become evident at $\sim 170$ keV; thus, in the energy region of interest for dark matter search ($\sim 0–10$ keV) it will be unlikely to achieve an effective particle discrimination based on the light yield, even with a substantial improvement of the light collection in comparison to this measurement. In the vicinity of the neutron capture a small family of events appears, with a slightly higher energy. There is currently no clear interpretation and further investigations will be carried out to understand its origin, which might be tied to a resonance in the cross section for the $^6\text{Li}(n,\alpha)^3\text{H}$ reaction. This family of events has not been observed in the LNGS measurement (see Sect. 7), but the neutron source employed in that case had an extremely reduced activity with respect to the above-ground measurement.

5 Dark matter results

As explained in Sect. 4, module $B$ was designed to study spin-dependent interactions of low-mass dark matter particles with nuclei of a LiAlO$_2$ crystal in a cryogenic measurement. A low threshold is a key parameter to reach this goal, due to the steep increase of expected dark matter recoils at lower energies. For this reason the TES was directly evaporated onto the LiAlO$_2$ surface, applying, for the first time, the CRESST technology on a crystal containing lithium.

A total of 22.2 h of data without any source (“background data”) were collected for module $B$ using a continuous DAQ with a sampling rate of 25 kHz. The events were triggered with a dedicated software based on the optimum filter [26].

The energy calibration is implemented using the 5.895 keV peak from the $^{55}\text{Fe}$ source, similar to the one used for the LD of module $A$. During the run, heater pulses of four different known amplitudes were injected to interpolate the energy calibration in the whole energy region of interest. The peaks corresponding to the heater pulses are identified in the dataset: each peak is fit with a Gaussian function which returns the mean and the error of the mean. Afterwards, the amplitude of heater pulses ($A_{\text{injected}}$) versus the amplitude measured by the TES ($A_{\text{phonon}}$) is plotted and the following function is fit to the data points:

$$A_{\text{phonon}} = p_0 \cdot \frac{p_1 \cdot A_{\text{injected}} \cdot I}{R_L + p_1 \cdot A_{\text{injected}}}$$

(3)

where $p_0$ is the gain of the SQUID, $I$ is the bias current of the TES, $R_L$ is the load resistor, and $p_1$ is a coefficient which translates the temperature change of the TES, induced by the heat pulse, into a variation of the TES resistance. Equation 3 is derived from the circuit scheme used to read out the TES [22]. For this measurement $I = 9\ \mu\text{A}$, while $R_L = 40\ \text{m}\Omega$; $p_0$ and $p_1$ are the free parameters of the fit. Finally, the mean value registered by the TES $A_{\text{phonon}} = (2379.2 \pm 0.7)$ a.u. corresponding to the 5.895 keV X-ray is used to convert $A_{\text{phonon}}$ to energy via Eq. 3. This description assumes that the TES resistivity changes linearly with the temperature in the energy interval considered ($0–6$ keV). With this method an accurate energy calibration (Fig. 6) was obtained taking into account the intrinsic non-linearity of the read-out scheme. The baseline resolution is $\sigma_{\text{baseline}} = (39.75 \pm 1.23)$ eV. The corresponding energy threshold for particle interactions with the target is $E_B = (213.02 \pm 1.48)$ eV, calculated by using the same method as presented in [27]. In this case, however, the total rate of counts in the noise above threshold (noise trigger rate) is set to $10^3$ counts/(keVkgday), two orders of magnitude lower than the observed event rate in the 1–5 keV range.
limits adopts the standard dark matter halo model, which framework presented in [5]. The calculation of the exclusion cle events only. At 5.895 keV the peak caused by the X-ray emission of $^{55}$Fe decay appears; the energy resolution at 5.895 keV is equal to $\sigma_{K_{a}} = (184.0 \pm 1.6)$ eV. The resolution for heat pulse events is equal to $\sigma_{HP_{1}} = (41.6 \pm 1.0)$ eV at 1.159 keV and $\sigma_{HP_{2}} = (57.0 \pm 1.6$ eV) at 11.537 keV. Below 300 eV there is a rise in the spectrum.

Figure 7 shows the calibrated energy spectrum of the 22.2 h background measurement. The X-ray peaks from $^{55}$Fe decay clearly emerge. A moderate rise of events below 300 eV is also evident. The energy resolution at 5.895 keV, calculated in the same way as for the LD of Module A, is $\sigma_{K_{a}} = (184.0 \pm 1.6)$ eV, significantly worse than the resolution for heat pulse events which is equal to $\sigma_{HP_{1}} = (41.6 \pm 1.0)$ eV at 1.159 keV and $\sigma_{HP_{2}} = (57.0 \pm 1.6$ eV) at 11.537 keV. This degradation in energy resolution for particle events is being investigated further. In the flat part of the spectrum, below the X-ray peaks, the background rate is of the order of 2 $\times$ 10$^{5}$ counts/(keV kg day), similar to the one observed in [28]. This high value is expected, since the detector is operated in an above-ground laboratory without any shielding or veto systems.

From the measured spectrum, dark matter exclusion limits for spin-dependent interactions are calculated. The energy region of interest ranges from $E_{B}^{H}$ to 4000 eV without applying any cut to the particle events registered by the detector. All the events with energies above 4000 eV contribute to the dead time, reducing the exposure from 22.2 to 17.2 h, corresponding to a total exposure of 2.01 $\times$ 10$^{-3}$ kg day, with an exposure for $^{7}$Li of 1.95 $\times$ 10$^{-4}$ kg day and an exposure for $^{27}$Al of 8.22 $\times$ 10$^{-4}$ kg day. The exclusion limits are calculated using Yellin’s optimal interval method [29,30] and are shown in Fig. 8. The baseline resolution of the detector $\sigma_{P_{baseline}}$ and the energy threshold $E_{B}^{P}$ are taken into account to evaluate the minimum value of dark matter mass for which it is possible to draw exclusion limits. These limits are valid for both proton-only interactions and for neutron-only interactions, as discussed in the theoretical framework presented in [5]. The calculation of the exclusion limits adopts the standard dark matter halo model, which assumes a Maxwellian velocity distribution and a local dark matter density of $\rho_{DM} = 0.3$ (GeV/c$^{2}$)/cm$^{3}$ [31]. Furthermore, $v_{esc} = 544$ km/s is assumed for the galactic escape velocity [32] and $v_{o} = 220$ km/s for the solar orbit velocity [33]. For the proton-only exclusion limits $\langle S_{p} \rangle = 0.4970$ for $^{7}$Li and $\langle S_{p} \rangle = 0.3430$ for $^{27}$Al are used, while for the neutron-only exclusion limits $\langle S_{n} \rangle = 0.0040$ for $^{7}$Li and $\langle S_{n} \rangle = 0.0296$ for $^{27}$Al [7,17] are used. The data analysis efficiency is computed generating a known flat energy spectrum of events. These events are created by superimposing the ideal detector response on recorded data and then processed with the same analysis chain used for the real data. The fraction of surviving events over the total simulated events at each energy bin represents the data analysis efficiency. Since the determination of the amplitude and the triggering are done in one step by the optimum filter and no further data selection criteria applied, in this case the data analysis efficiency is equivalent to the trigger efficiency.

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6 Experimental setup at LNGS

After the successful tests at MPP, the bulk of the original LiAlO$_2$ crystal sample was mechanically polished obtaining a 373 g crystal. Such crystal size is ideal to study the crystal radiopurity and to assess the feasibility of using LiAlO$_2$ crystal as a monitor for the neutron flux in a shielded experimental setup. For this reason, this crystal was used in a new detector module, module C, which was installed in the MPP Test-Cryostat facility located in the underground laboratory of Laboratori Nazionali del Gran Sasso (LNGS), under 3600 m water equivalent overburden to shield against cosmic radiation [41].

As visible in Fig. 9, an NTD [21], a (5 × 5 × 1) mm$^3$ Si carrier with a thin gold stripe heater deposited on it, and a CaWO$_4$ carrier crystal on which a CRESST-II TES had been evaporated [42] are both glued to the top surface of the LiAlO$_2$ crystal. The NTD and the CRESST-II TES are both being used as phonon sensors. This choice is motivated by the fact that the NTD has a higher dynamic range than the TES, while the TES can generally achieve a lower energy threshold than the NTD. Therefore, with this detector module it is possible to study both the low energy part of the spectrum (≈ 1 keV) and the high energy part (≈ 10 MeV). This allows the potential setting of competitive limits for spin-dependent dark matter search and the detailed study of the neutron capture by $^6$Li during the same measurement. The crystal was held in position inside a copper holder using three PTFE clamps on the bottom and three on the top. Reflective foil was used to surround the crystal, in order to maximize light collection. A CRESST-II light detector [43] was facing the top surface of LiAlO$_2$, completing the detector module.

The MPP Test-Cryostat facility is located in the corridor connecting Hall A and Hall B of LNGS. The model of dilution refrigerator installed in this facility is the same as the one used for the above-ground measurement at MPP. The detector module operated in this dilution refrigerator employs the same kind of wiring, NTD readout, and TES readout as in the previous above-ground measurement.

7 Neutron and radiopurity measurements at LNGS

The detector operation of module C at LNGS was divided into two parts: one focused on the efficacy of measuring neutrons, the other on measuring the radioactive impurities in the crystal. For these type of measurements, the data collected with the NTD (that does not saturate in the energy region of interest) and the CRESST-II light detector have been analyzed.

The CRESST-II TES was also simultaneously operated as a phonon sensor to study the low-energy part of the spectrum (< 1 MeV).

At the beginning of the run an AmBe neutron source emitting ∼ 10 neutrons/s was installed at a distance of ∼ 60 cm from the center of the dilution refrigerator and 13.1 h of data were collected. To ensure the stability of the NTD sensor, heater pulses with seven different amplitudes were injected, two of which were close to the energy region of interest for the neutron capture by $^6$Li (Eq. 1). The detector response was calibrated using these heater pulses and the 4.78 MeV peak corresponding to the neutron capture. After calibration, the energy resolution at 4780 keV is $\sigma_{\text{capture}} = (18.3 \pm 1.02)$ keV. In Fig. 10, the scatter plot of QF versus the energy registered by the NTD for all the events recorded during the neutron measurement is presented.

In this plot, the neutron capture peak shows a higher QF than the events originating from α decays. These two classes of events are used to build two histograms (Fig. 11): neutron capture events are selected from an energy interval of $\pm 3\sigma_{\text{capture}}$ centered around 4780 keV, while all other events above 4 MeV are considered α events. It is possible to see that the two distributions are partially overlapping. However, even with a simple cut on the QF value one can exclude

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5 GP 12 Allzweck-Epoxidkleber.
6 3M’s Vikuiti™ Enhanced Specular Reflector.
Fig. 10  QF versus the energy registered by the NTD sensor for 13.1 h of effective live time in the presence of a weak AmBe source. For energies \( \lesssim 2.6 \) MeV it is possible to see the \( \beta/\gamma \) band which was used to normalize the QF. At energies \( \gtrsim 3 \) MeV and for lower QF values, multiple families originated by \( \alpha \) decays and one prominent line at 4.78 MeV corresponding to the neutron capture of \(^6\)Li can be seen.

Fig. 11  Distribution of QF values for events originated by \( \alpha \) decays with a mean value of 0.38 \( \pm 0.04 \) (red) and distribution of QF for neutron capture events with a mean value of 0.44 \( \pm 0.03 \) (blue).

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the vast majority of unwanted \( \alpha \) decay events: if only events with a QF \( > 0.44 \) (the mean value of the neutron capture distribution) are accepted, 93.3\% of \( \alpha \) events are cut while halving the detection efficiency for the neutron capture. The efficiency in discarding \( \alpha \) events can then also be considerably increased defining a cut on the energy detected by the NTD phonon sensor: clearly, this cut is more effective the higher the energy resolution of the NTD.

In a low-background environment only a few neutron events are expected, while the number of alpha events depends on the radiopurity of the detector. This means that there would probably be not enough events to build two distributions based on the QF values. However, it is possible to perform a neutron calibration and then, based on the data, define a region where neutron events are expected during the background data campaign. From the total number of events inside this region, it is then feasible to quote a neutron flux value (or upper limit) with the respective uncertainty.

The long term goal for CRESST is to directly detect neutrons inside the experimental setup using a specifically designed detector based on a lithium-containing crystal, thereby providing a relevant input to the background model of the experiment. From this data, using dedicated Monte Carlo simulations, the total neutron flux (or an upper limit) can be assessed while also possibly reconstructing the energy spectrum of the incoming neutrons. The measurement presented in this work is a first step in this direction.

After the neutron measurement, the AmBe source was removed to measure the radiopurity of the crystal. In this case, a 58.4 h background measurement was carried out. After stability and data quality cuts, the effective measuring time is 35.6 h. In this measurement it was not possible to use the neutron capture peak to calibrate the NTD response, but the heater pulses that were previously calibrated were used instead. In Fig. 12, the energy spectrum measured by the NTD is shown without cuts. From this spectrum, at least 6 different peaks due to \( \alpha \) decays in the 4–7 MeV region can be distinguished. After a careful evaluation, it can be assumed that three radioactive parents are inducing the peaks highlighted: \(^{210}\)Po, \(^{226}\)Ra, and natural uranium. The respective calculated activities are listed in Table 1. In principle, \(^{226}\)Ra should be part of the \(^{238}\)U decay chain, but it is not possible to correctly match the respective activities. One straightforward explanation is that \(^{226}\)Ra and \(^{238}\)U are not in secular equilibrium; as such the two contaminants are treated as separate parents of their respective decay chain. In fact, in the case of the secular equilibrium the peak centered around 4.86 MeV is expected to be \( \sim 3 \) times more populated than the \(^{238}\)U peak, due to the summing of \(^{226}\)Ra, \(^{230}\)Th, and \(^{234}\)U activities. However, this peak is only 1.43 times more populated.
the 238\(^{\text{U}}\) peak and equal, well within 1 sigma, to the sum of 222\(^{\text{Rn}}\) (0.962 ± 0.142 \text{ mBq}) and 238\(^{\text{U}}\) activities. One explanation which can fit well the data is that 226\(^{\text{Ra}}\) and its daughters are in secular equilibrium and have the same activities, while we do not observe the daughters of 238\(^{\text{U}}\) and 235\(^{\text{U}}\) decay chains. The activities ratio of the uranium isotopes are roughly as expected for the presence of natural uranium, only the activity of 235\(^{\text{U}}\) is slightly higher than expected, but within 2 sigma. It has to be noted that the 235\(^{\text{U}}\) peak is the least populated and so the most affected by statistical uncertainties. The uranium peaks appear to be broader than the peaks caused by the 226\(^{\text{Ra}}\) daughters. This could signal that the uranium might be present both internally and on the surfaces of the crystal, while 226\(^{\text{Ra}}\) might prevalently be an internal contamination. This observation, combined with the break of the secular equilibrium between 238\(^{\text{U}}\) and 226\(^{\text{Ra}}\), could point at two contaminations at different stages of the crystal production and handling, one related to 226\(^{\text{Ra}}\) and one due to natural uranium.

In addition to the 214\(^{\text{Bi}}\)–214\(^{\text{Po}}\) decays, two peaks can be attributed to the daughters of 226\(^{\text{Ra}}\): 218\(^{\text{Po}}\) and 222\(^{\text{Rn}}\). Finally, a modest contamination of 210\(^{\text{Po}}\) is also observed.

The total number of events above 3 MeV is 483: this means an upper bound on the total alpha activity of (10.1 ± 0.5) \text{ mBq/kg} for this particular LiAlO\(_2\) crystal. Considering this value, the radioruption of this crystal is ~ 3 times worse than the most radiopure CaWO\(_4\) crystal produced within the CRESST Collaboration (TUM40) [44], but in line with standard commercial CaWO\(_4\) crystals. The goal for the future is to drastically improve the radioruption of LiAlO\(_2\), starting from a careful selection of the raw materials used for the crystal growth, and the material used for cutting and polishing. Additionally, a 20.8 \text{ h} calibration using a 241\(^{\text{Am}}\) gamma source installed close to the outer shield of the dilution refrigerator was carried out to test the performance of the CRESST-II TES [45]. During the calibration and the background measurement, heater pulses with nine different amplitudes were injected. The 59.54 \text{ keV} gamma peak from the 241\(^{\text{Am}}\) source used for the energy calibration has a resolution of \(\sigma_{\text{Am}} = (3.044 ± 0.074) \text{ keV}\). Similarly for the TES calibrations presented before, this peak and the peaks corresponding to the injected heater pulses are used to accurately calibrate the detector response at different energies. The sensor has an energy threshold of (2.601 ± 0.126) \text{ keV}, considerably higher than that achieved in the measurement performed above-ground with a smaller LiAlO\(_2\) crystal: this is expected due to the large increase in mass as showed by the scaling law described in [46].

### 8 Conclusions

This work details the results of three different detectors, all of which employ a LiAlO\(_2\) target crystal, a material that has never been employed in cryogenic experiments thus far. The cryogenic properties of the material were tested in an above-ground laboratory with a 2.8 g crystal and new limits on spin-dependent dark matter interactions are set with a crystal instrumented with a TES deposited on LiAlO\(_2\). A large-size detector with a mass of 373 g was operated in an underground cryogenic facility at LNGS in the presence of a weak neutron source, in order to assess the feasibility to monitor the neutron flux directly inside cryogenic setups. The results presented in this work demonstrate the high potential of LiAlO\(_2\) crystals as cryogenic detectors in the field of low-background applications and contribute to the ongoing search for dark matter.

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**Data Availability Statement** This manuscript has associated data in a data repository. [Authors’ comment: The spectrum used for the dark matter limit calculations and the limits are available at https://arxiv.org/abs/2005.02692].

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