Additive manufacturing processes are considered advanced manufacturing methods. It would be possible to produce complex shape components from a computer-aided design model in a layer-by-layer manner. As one of the complex geometries, lattice structures could attract lots of attention for both medical and industrial applications. In these structures, besides cell size and cell type, the microstructure of lattice structures can play a key role in these structures’ mechanical performance. On the other hand, heat treatment has a significant influence on the mechanical properties of the material. Therefore, in this work, the effect of the heat treatments on the microstructure and mechanical behaviour of Ti-6Al-4V lattice structures manufactured by electron beam melting was analysed. The main mechanical properties were compared with the Ashby and Gibson model. It is very interesting to notice that a more homogeneous failure mode was found for the heat-treated samples. The structures’ relative density was the main factor influencing the mechanical performance of the heat-treated samples. It is also found that the heat treatments were able to preserve the stiffness and the compressive strength of the lattice structures. Besides, an increment of both the elongation at failure and the absorbed energy was obtained after the heat treatments. Microstructure analysis of the heat-treated samples confirms the increment of ductility of the heat-treated samples with respect to the as-built one.

Keywords Additive manufacturing · Electron beam melting · Lattice structures · Heat treatment

1 Introduction

Additive manufacturing (AM) is “a process of joining materials to obtain components from 3D model data using a layer upon layer approach” [1–5]. This approach enables the successful production of parts without design constraints, allowing the integration of components and the use of topologically optimized and lightweight structures [6–8]. Therefore, over the past years, various companies and industrial sectors have applied this technology to benefit from its advantages [9, 10]. In general, metal AM processes can be divided into directed energy deposition (DED) and powder bed fusion (PBF) processes [11]. Among the latter, the electron beam melting (EBM) process, as a PBF method, has received considerable interest in the aerospace and medical sectors [10, 12]. The main driver for aerospace applications is represented by the possibility to process the materials that their processability with the other technologies faced with several challenges [13]. Regarding the medical sector, the EBM process is able to produce tailored implants, ensuring better bio-compatibility and improving the interaction between the prosthesis and prior tissues [14, 15].

Ti-6Al-4V is one of the most processed materials by EBM technology, which can open new doors in the manufacturing of this particular alloy [16]. Traditionally, Ti-6Al-4V parts suffer from high-density inclusions (HDI), low-density inclusions (LDI) and surface oxidation [17]. The EBM process can avoid the first two defects mentioned above and limit the latter due to its vacuum working conditions [16]. On the other hand, during the production of Ti-6Al-4V alloy via the EBM process due to the presence of a preheating phase before the melting, the temperature inside the building chamber reaches values of 650–750 °C for this specific alloy [16, 18, 19]. These working conditions ensure small thermal shrinkages,
and the powder bed results in enough strength to support the construction of the overhang part and limiting the use of supports [20, 21]. Therefore, EBM makes possible the production of so-called micro-architected components. These parts, also known as cellular structures, are of considerable interest because of the opportunity to achieve a singular combination of lightness and high mechanical properties compared to their corresponding bulk ones [22, 23]. In general, this class of materials includes foams and lattice structures [24]. Lattice structures are widely produced by EBM thanks to the possibility to achieve high specific strength [25], oxidation resistance [25, 26] and biocompatibility with the human tissues [14, 26, 27]. These structures, also known as cellular, reticulated or truss, have been defined as repetitions in a unit elementary cell [22]. The three main factors affecting the properties of cellular solids that have been identified by Ashby [28] are: (1) the material of which is made, (2) the cell topology and shape and (3) the relative density. The first affects the mechanical, electrical and thermal properties, while the second, following the Maxwell criterion [29], distinguishes bending-dominated structures from strength-dominated structures. The relative density is given by the ratio between the density of the cellular material ($\rho_s$) and the density of the bulk material ($\rho_b$) [24]. The relative density and the type of unit cell strongly affect both the cooling rate of the material during the solidification and the load distribution during its working conditions. High cooling rate values may lead to forming a microstructure mainly composed of $\alpha'$ martensite, in contrast with the bulk material [18, 25, 30–37]. Up to date, several studies have been focused on evaluating the performance of lattice structures. For instance, Del Guercio et al. [38] have analysed the mechanical performance of three different types of lattice structures: (i) Dode thin, (ii) G-Structure 3 and (iii) Rombi-dodecahedron. The structures have been tested under compressive at ambient temperature are conducted with the aim to correlate the effect of different heat treatments on the lattice structures. Therefore, the aim of the present study is to deeply analyse the stress-strain trend: (1) elastic behaviour of the lattice structures (a linear segment), (2) progressive collapse of the layers up to the point where (3) the structure has the same behaviour of the bulk material. The limit of the elastic behaviour is the failure point, namely, when the stress reaches the ultimate compressive strength ($UCS^*$), and the strain reaches the elongation at failure ($A^*$). Typically, the failure mode in these components is a brittle fracture at $45^\circ$, as reported in the literature [36–42]. The lattice structures manufactured in larger cell sizes showed the worst mechanical performances, in terms of both Young’s modulus and $UCS^*$, with respect to those produced with smaller cell size [38, 41, 43, 44]. Ashby and Gibson [24] proposed a model to describe the mechanical performances of lattice structures, in which a generic relative property can be expressed, in a bi-logarithmic diagram, as a linear relationship of the lattice relative density. Thereafter, several studies have used Ashby and Gibson’s [24] model to fit their evaluated mechanical properties experimentally. Additionally, Del Guercio et al. [38] proved that the absorbed energy up to failure ($W^*$) also follows an Ashby-Gibson-like relationship. However, they also showed that the relative density is not totally descriptive of the mechanical behaviour of the lattice structure. All in all, several efforts have been made to evaluate the effect of cell type and cell size on the compressive behaviour of the EBM Ti-6Al-4V lattice structures. However, far too little attention has been paid to the effect of different heat treatments on the mechanical properties of the EBM lattice structures. This can potentially open new opportunities and widen the range of application of Ti-6Al-4V lattice structures. Several studies have shown the potential of the heat treatment on Ti-6Al-4V bulky parts. Several works proved that the overall porosity of the parts made by EBM could be reduced by applying a hot isostatic pressing (HIP) treatment that is generally conducted at 920 °C for 2 h [34, 45–47]. Tammas-Williams et al. [46] showed that the temperature in an annealing heat treatment enables the formation of new voids or pore regrowth during the heat treatment after HIP. De Formanoir et al. [31] showed that thermal cycles significantly affect the mechanical response of the bulk parts. They studied two different heat treatments: the first was conducted below $\beta$-transus (transition temperature between the $\alpha$ and $\beta$ phases is equal to 995 °C [18]) at a specific temperature of 950 °C for 60 min. On the other hand, the second one was conducted at 1040 °C for a total time of 30 min. The results showed that at higher temperatures, the microstructure changed due to solid-state diffusion and coarsening of the plates of the $\alpha$ phase. As far as the response of lattice structure to heat treatment is concerned, far too little attention has been paid. As an example, Epasto et al. [48] studied the compressive behaviour of Ti-6Al-4V cellular structures manufactured by EBM, which were heat-treated to reduce residual stress. They concluded that the possible presence of residual stresses does not significantly affect the compressive behaviour of Ti-6Al-4V lattice structures manufactured by the EBM process. On the other side, in a new approach on the design of the complex shape components, a mix of lattice and bulk structures is generally used in order to reduce their weight while keeping their mechanical performance as high as their fully bulk ones. Therefore, the aim of the present study is to deeply analyse the effect of different heat treatments on the lattice structures. With this scope, the microstructure and mechanical properties of the Ti-6Al-4V lattice structures produced by EBM process in the as-built and heat-treated states are compared. Isothermal heat treatments were performed below and above the $\beta$-transus. Compressive tests at the ambient temperature are conducted with the aim to correlate...
the mechanical performance to the microstructure variation induced by the heat treatments.

2 Materials and methods

2.1 Lattice design and production

In this work, the same lattice designs of our previous work were used to compare the response of the lattice structures in the as-built and heat-treated states [38]. For this reason, three different unit cell topologies were studied: (i) Dode thin, (ii) G-Structure 3 and (iii) Rombi-dodecahedron (Figure 1).

These structures were selected among the standard lattice unit cells presented in the Materialise Magics 21.11 software database. This choice enables the analysis of different relative densities and strut sizes. Compressive samples (Figure 2) were designed in a cylindrical shape with diameter and height of 20 mm and 30 mm height, respectively.

The lattice structures were designed between two bulk caps with a thickness of 2 mm in order to provide a uniform distribution of the load during the compressive tests. As a result, the lattice segment’s total height, without considering these disks, was 26 mm. Each unit cell has been designed in three different sizes: 4, 7 and 10 mm. With the specific aim to guarantee a robust experimental analysis, each cell typology and size were produced in three replicas. Since the overall thermal conditions analysed were three, 81 samples were produced in a single job. All the specimens were produced unattached to the start plate with the addition of support structures to avoid microstructure modifications. They were also spaced along the build direction axis to have a uniform temperature distribution during each build phase. The build job was prepared using Magics 21.11 and processed by the EBM build processor 5.0 with a Ti-6Al-4V standard theme for the Arcam A2X system. The layer thickness was set equal to 50 \( \mu \text{m} \). The adopted process parameters are listed in Table 1.

Standard Arcam Ti-6Al-4V powder with an average size of 75 \( \mu \text{m} \) was used as a feedstock material to produce the lattice structures using an Arcam A2X system. The chemical composition of the starting powder is reported in Table 2.

After the production, the entire build has been cooled down inside the Arcam A2X chamber. Subsequently, all the residual powder was removed from the samples using a blasting process with compressed air at 4 bar and the same Ti-6Al-4V powder used for the production.

2.2 Heat treatments

In order to track the effect of heat treatment temperature on the mechanical performance of the lattice structure, two different heat treatments, below and above the transus temperature, were performed. Figure 3 depicts the temperature-time cycle used in this work to heat treat the Ti-6Al-4V lattice structures. Both heat treatments were conducted for 60 min under vacuum to avoid oxidation at high temperatures. Both thermal conditions were compared to the as-built state. The mechanical properties were determined through the compressive tests, as illustrated in Figure 2. The compressive stress-strain curves and the calculated mechanical properties are presented in Table 3.
cycles were performed with the same heating and cooling rates while the first heat treatment, named HT1 (blue line in Figure 3), was performed at 950 °C, below β-transus, and the second heat treatment, named HT2 (red line in Figure 3), was performed at 1040 °C, above β-transus. The as-built condition was named as NTH.

2.3 Compression test

The mechanical behaviour of the lattice structures is analysed under uniaxial compression tests using a strain velocity of 2 mm/min up to the full collapse of the structure according to ISO 13314. In order to evaluate the stress/strain curves, loads and displacements were converted using Eqs. 1 and 2:

\[
\sigma = \frac{P}{A_0} \quad (1)
\]

\[
\varepsilon = \frac{\delta}{l_0} \quad (2)
\]

\(P\) represents the load and \(\delta\) is the displacement measured during the compression test; \(A_0\) represents the area of the whole structure, namely the area of a 20-mm diameter circle; \(l_0\) is the height of the lattice part of each sample (26 mm). Figure 4 depicts a qualitative stress/strain trend.

In a stress/strain diagram, the area under the curve and delimited by the failure point represents the absorbed energy up to failure per unit of volume. The total absorbed energy up to failure (\(W^*\)) can be evaluated according to Eq. 3, where \(V^*\) is the actual volume of a lattice structure.

\[
W^* = \int_0^{\delta^*} \sigma \varepsilon \cdot V^* \quad (3)
\]

The compressive Young’s modulus (\(E^*\)) is represented by the slope of the linear trend (red line in Figure 4). Considering two points in this line, \(E^*\) can be evaluated using Eq. 4.

\[
E^* = \frac{\sigma_2 - \sigma_1}{\varepsilon_2 - \varepsilon_1} \quad (4)
\]

Table 2  Chemical composition of the as-received Ti-6Al-4V powder

| Composition (wt.%) | Al  | V   | C   | Fe  | O   | Ti   |
|-------------------|-----|-----|-----|-----|-----|------|
| Nominal           | 6.1 | 3.9 | 0.03| 0.1 | 0.15| Bal. |
| Standard          | 5.5–6.7 | 3.5–4.5 | <0.1| <0.3| <0.2| Bal. |

2.4 Characterization

By the subtraction of the mass of the upper and bottom cup from the total weight of the sample, the relative density (\(\rho^*/\rho_s\)) of each structure was evaluated from the ratio between the density of the lattice structure (\(\rho^*\)) and the nominal density of the bulk material (\(\rho_s\)). Table 3 lists the measured and calculated data for each cell topology and size.

For microstructure observations, all samples were first cut perpendicular to the building direction, then mounted, ground and polished according to the standard procedures for Ti alloys’ metallography [12]. The polished samples were etched using Kroll’s reagent (2% HF, 4% HNO₃ in distilled water). A Phenom table-top scanning electron microscope (SEM) equipped with an EDS detector was used to evaluate the microstructure.

3 Results and discussion

3.1 Mechanical properties

Figure 5 compares the compressive behaviour of the as-built Ti-6Al-4V lattice structures with those of the heat-treated ones. As designed, three replicas of each condition were tested to evaluate the repeatability of the results. For all conditions, a high degree of repeatability was found. Therefore, the subsequent comparisons were made by considering the average of the three measurements. As an example, Figure 5a depicts the three replicas built with the geometry structure II and tested under the thermal heat treatment HT1.
As discussed above, the compressive trend of the as-built lattice structure consisted of three major parts. This behaviour was also observed in the heat-treated samples produced with different cell size combinations and types. Figure 5b, c compares the compressive stress-strain for the geometry structure II in three different states: as-built (NTH), heat-treated below (HT1) and above (HT2) the $\beta$ transus temperature. As can be seen, the compressive behaviour of the heat-treated samples was similar and had a softer trend with respect to the as-built sample. The second segment of all the curves still characterized by a plateau region in multiple stress fluctuations can be observed, standing for the layers’ collapsing. The heat-treated samples showed a less pronounced stress change in the second segment of the compressive trend. As a consequence, the lattice structure had more ductile behaviour. Contrary to the as-built samples, the heat-treated samples did not show the brittle fracture with bands at 45° with respect to the horizontal plane (Figure 6c). Both heat-treated samples showed a more uniform failure mode, with the progressive and homogeneous collapse of the layers (Figure 6d). These findings are in very good agreement with the literature results [37, 49]. The barrelling effect was also observed during the conduction of the compression tests in the heat-treated samples that have no failure band formation at 45° (Figure 6d).

Since all the layers collapsed on the top of each other, the last part of the compression behaviour is characterized by the elastic behaviour of the bulk material in all the three analysed thermal conditions (NTH, HT1 and HT2). Overall, since after the failure point, the stress-strain trends of HT1 and HT2 were generally higher than the NTH trend, it can be stated that lattice structures showed a ductility enhancement in the heat-treated conditions.

Table 4 lists the average values of the analysed mechanical properties for each design configuration and in each thermal condition. As can be seen, no significant changes between the as-built and the heat-treated samples can be observed in terms of Young’s modulus and $UCS^*$ of the lattice structure. This result highlights the possibility of performing the heat treatments on the structure without losing their mechanical performances. The elongation at failure ($A^*$) results showed a sharp increment in the heat-treated conditions. Owing to the preservation of compressive strength, this variation proves a much more ductile behaviour of the heat-treated structure with respect to the as-built one. As far as the absorbed energy up to failure ($W^*$) is concerned, the heat treatments caused an increment of this property. This increment might be a consequence of the microstructural effect of the lattice structures that can play a key role in their mechanical performances. In fact, as mentioned earlier, a much more ductile behaviour of the heat-treated structure with respect to the as-built one resulted in higher absorbed energy in these samples. As also demonstrated in previous works [38], this property is strongly affected by the variation of $UCS^*$ or $A^*$. In this case, $W^*$ values are influenced by the high variation of $A^*$. The increment of $W^*$ proves the high absorbed energy by the treated lattice and, therefore, the ductility enhancement compared to the as-built condition.

It is well documented that the mechanical performance of lattice structures decreases mainly by increasing the unit cell size [38]. Table 4 shows the same trend for the lattice in the heat-treated conditions. As can be seen, the unit cell size increment caused a reduction in mechanical properties. The elongation at failure did not show any clear change by increasing the unit cell size (Table 4). It is interesting to notice that all geometries in all cell sizes showed the same trend of $E^*$, $UCS^*$, $W^*$. As an example, Figure 7 reports graphically the values included in Table 4 for the structure I in all sizes.

![Fig. 4 Qualitative stress/strain compressive trend of a generic lattice structure](image)

**Table 3** Average values of the weight of the lattice and relative densities

| Structure | I       | II       | III      |
|-----------|---------|----------|----------|
| Size (mm) | 4       | 7        | 10       |
| $m_{\text{lat}}$ (g) | 5.832   | 3.139    | 2.018    |
| $\rho^*/\rho_s$ (%) | 16.155  | 8.695    | 5.591    |
| $V^*$ (mm$^3$) | 1319.532 | 710.180  | 456.661  |

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Figure 8 depicts the effect of the unit cell type on the HT1 and HT2 samples designed with a 4-mm unit cell size. As can be clearly seen, structure I showed the worst mechanical performance, while structure II was the best one. Considering the elongation at failure, the structure I showed the highest values. These trends were not consistent with the ones observed for samples designed with the 7-mm and 10-mm unit cell sizes. As previously observed for the as-built condition [32], this result confirms that the unit cell size has a more significant influence on the mechanical behaviour of the lattice structures.

The dependency between the relative density and the mechanical properties can also be derived for the heat-treated samples. Figure 9 demonstrated the values of $E^*$, $UCS^*$ and $W^*$ for all the thermal conditions and each design as a function of the relative density of the structure. As can be seen, the sample designed with the geometry structure I with the unit cell of dimension 10 mm (Structure I-10) had the lowest relative density and showed the minimum of $W^*$, $E^*$ and $UCS^*$ in each thermal condition. The structure II-4 had the highest relative density and showed the best values of the analysed mechanical properties in all the NTH, HT1 and HT2 conditions. In general, it can be observed that the mechanical performances of lattice structures, for the analysed indexes, increase by increasing the relative density of the structures.

According to the Ashby and Gibson model [24], Young’s modulus has a linear relationship in a bi-logarithmic diagram with respect to the relative density:

$$\frac{E^*}{E_S} = C_1 \left( \frac{\rho^*}{\rho_S} \right)^n$$

(5)

$E_S$ is the stiffness of the bulk material (which for the bulk Ti-6Al-4V alloy was chosen equal to 120 GPa [44]), $C_1$ and $n$ are constants equal to 1 and 2, respectively. Figure 10 shows the experimental results for each of the analysed thermal conditions compared with the theoretical one of the Ashby and Gibson model [24] (black line). For each design, the performed heat treatment had no significant effect on the values of Young’s modulus. The interpolation of the experimental data highlights the trend for each of the studied thermal conditions. According to our previous work [38], the values of the constants $C_1$ and the exponent $n$ for the samples in the as-built conditions are equal to 0.301 and 2.493, respectively. Regarding the HT1 condition, $C_1$ is equal to 0.280, and $n$ is equal to 2.365. For the HT2 condition, the $C_1$ and $n$ are equal to 0.219 and 2.168, respectively. The comparison between the experimental data and the theoretical one showed a constant deviation where the values calculated according to the Ashby and Gibson model [24] were always higher. The difference can be explained by the fact that the number of sharp edges and corners in a repetitive structure, as in the lattice structure, was higher than the one present in stochastic structures as in the Ashby case Gibson analyses [24]. These geometrical features acted as stress concentration points that lower the lattice’s overall stiffness with respect to stochastic one [24].

Similar to Young’s modulus, also the $UCS^*$ can be described by a relationship with respect to the relative density:

$$\frac{UCS^*}{UCS_S} = C_5 \left( \frac{\rho^*}{\rho_S} \right)^m$$

(6)

where $UCS_S$ is the ultimate compressive strength of the bulk material (assumed equal to 1000 MPa) and $C_5$ and $m$ are constants equal to 0.3 and 1.5, respectively [24].

Figure 11 shows the comparison between the experimental trends and the theoretical ones. According to the findings for the as-built Ti-6Al-4V lattice structures [38], $C_5$ and $m$ were assumed equal to 0.744 and 2.012, respectively. For the heat-treated samples, $C_5$ and $m$ were calculated. $C_5$ is equal to 0.697 and 0.806, while $m$ is 1.941 and 2.100 for the HT1 and HT2 conditions, respectively. Different from the $E^*$, the experimental trends of $UCS^*$ were closer to the Ashby-Gibson model [24].

Following the findings reported for the as-built Ti-6Al-4V lattice structures [38] about the existing linear relationship in a bi-logarithmic diagram between the relative $W^*$ and the
relative density in the as-built samples, a linear interpolation was also searched in the case of heat-treated samples. According to previous works [38], the absorbed energy up to failure can be described by the following equation:

$$\frac{W^*}{W_S} = C \left( \frac{\rho^*}{\rho_S} \right)^x, \quad (7)$$

where $W_S$ represents the absorbed energy up to the failure of the bulk material, while $C$ and $x$ are constants and equal to 3.153 and 2.472, respectively, for lattice in the as-built conditions [38]. Regarding the HT1 and HT2 conditions, the $C$ is equal to 11.372 and 16.363, while the $x$ is 3.101 and 3.437, respectively. The increment of the constants in the heat-treated condition compared to the as-built one shows the enhancement in ductility of the material after the heat treatment. Figure 12 compares the experimental trends.

All in all, from a mechanical point of view, it is possible to state that lattice structures in the heat-treated conditions are able to preserve stiffness and strength with the increasing of $A^*$.
a consequence of $W^*$ also explains the change in failure mode, which was shown in Figure 6.

### 3.2 Microstructure analysis

In general, the EBM process is able to guarantee a unique microstructure due to its rapid solidification and high temperature in the chamber. In particular, preferred crystallographic orientations and, thus, specific mechanical features can be achieved. In addition, different from other metal AM techniques, the high temperature in the building chamber is able to stop the solidification process at temperatures far higher with respect to the ambient temperature [18]. This specific feature in some unique microstructural characteristics can hardly be achieved through the laser-based techniques. Post-manufacturing heat treatments can change the obtained microstructure, guaranteeing a vast variety of mechanical features. Despite this, the rapid solidification of the EBM process can also result in micro-segregation and formation of metastable phases. Previous studies [25, 32] have reported indeed the presence of hexagonally packed acicular martensite known as the $\alpha'$ phase. However, the typical microstructure for the as-built condition consists of acicular $\alpha$ (known as Widmastätten platelet structure) surrounded by the $\beta$ phase. This variety of microstructure achieved in the as-built condition shows the effect of the design of samples on the solidification of Ti-6Al-4V samples. Thin structures may show a more severe thermal gradient, resulting in a diffusionless transformation with the formation of $\alpha'$ martensite. Additionally, the heat transported during the melting of the next layer on the previous one may promote the diffusion, and a solid-state transformation may lead to the dissolution of the cited metastable phase. Del Guercio et al. [38], showed that in the as-built condition, the lattice structures are characterized by the typical microstructure of EBM Ti-6Al-4V, which is composed of columnar grains of the prior $\beta$ phase growing in the building direction and Widmanstätten $\alpha$ platelets. Additionally, the cell type and size play a negligible role in

![Fig. 7 Main mechanical properties for the specimens designed with the structure I in all the three unit cell sizes for the (a) HT1 and (b) HT2 conditions](image-url)

#### Table 4 Average properties of each different sample’s unit cell type and size evaluated for each thermal condition

| Struct. | Cell size (mm) | $E_{\text{NTH}}^*$ (GPa) | $E_{\text{HT1}}^*$ (GPa) | $E_{\text{HT2}}^*$ (GPa) | UCS$_{\text{NTH}}^*$ (MPa) | UCS$_{\text{HT1}}^*$ (MPa) | UCS$_{\text{HT2}}^*$ (MPa) | $A_{\text{NTH}}^*$ (%) | $A_{\text{HT1}}^*$ (%) | $A_{\text{HT2}}^*$ (%) | $W_{\text{NTH}}^*$ (kJ) | $W_{\text{HT1}}^*$ (kJ) | $W_{\text{HT2}}^*$ (kJ) |
|---------|----------------|--------------------------|--------------------------|--------------------------|----------------------------|----------------------------|----------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|--------------------------|
| I       | 4              | 0.339                    | 0.357                    | 0.351                    | 19.145                     | 17.067                     | 17.782                     | 10.947                   | 14.850                   | 13.300                   | 1.532                    | 2.393                    | 1.907                    |
|         | 7              | 0.074                    | 0.087                    | 0.083                    | 4.742                      | 4.478                      | 4.624                      | 10.644                   | 12.254                   | 13.606                   | 0.201                    | 0.253                    | 0.288                    |
|         | 10             | 0.036                    | 0.035                    | 0.032                    | 2.262                      | 2.260                      | 2.203                      | 11.951                   | 14.729                   | 12.954                   | 0.081                    | 0.102                    | 0.088                    |
| II      | 4              | 2.264                    | 2.401                    | 2.304                    | 81.882                     | 82.658                     | 82.694                     | 8.231                    | 11.031                   | 10.721                   | 7.321                    | 13.462                   | 13.569                   |
|         | 7              | 0.717                    | 0.770                    | 0.901                    | 32.435                     | 32.486                     | 33.869                     | 7.392                    | 12.627                   | 12.862                   | 2.248                    | 4.594                    | 4.704                    |
|         | 10             | 0.659                    | 0.711                    | 0.707                    | 28.665                     | 26.851                     | 26.583                     | 7.973                    | 8.408                    | 8.436                    | 1.803                    | 2.006                    | 1.786                    |
| III     | 4              | 1.560                    | 1.683                    | 1.639                    | 60.034                     | 58.940                     | 56.156                     | 8.077                    | 10.823                   | 11.031                   | 4.837                    | 8.408                    | 7.692                    |
|         | 7              | 1.285                    | 1.427                    | 1.548                    | 54.877                     | 47.653                     | 47.713                     | 8.331                    | 11.208                   | 9.350                    | 4.964                    | 6.795                    | 5.659                    |
|         | 10             | 0.967                    | 1.208                    | 1.237                    | 39.691                     | 40.287                     | 39.291                     | 7.186                    | 7.767                    | 7.800                    | 2.836                    | 3.184                    | 3.051                    |
Fig. 8 Main mechanical properties for the specimens designed with the 4-mm unit cell size in all the three structure types in the (a) HT1 and (b) HT2 conditions.

Fig. 9 Variation of the mechanical properties according to the relative density of the structure in the NTH (grey), HT1 (blue) and HT2 (red) conditions.
the microstructure of specimens. The resulting microstructure of as-built samples showed an average thickness of the $\alpha$ platelets in the range between 1 $\mu m$ and 2 $\mu m$.

Figure 13 depicts SEM images for the specimens with the geometry corresponding to structure I and all unit cell sizes in the HT1 (a-b-c) and HT2 (d-e-f) conditions. The microstructure of heat-treated samples is still composed of a combination of $\alpha$ and $\beta$ phases. Comparing the heat-treated conditions, no important microstructure changes are observed. Specifically, the width of the $\alpha$ platelets seems not to be influenced by the unit cell type. Thus, the microstructure of lattice specimens in the heat-treated conditions depends only on the parameters adopted during the thermal cycle. This result is a direct consequence of the equilibrium conditions guaranteed by the used heat treatments. Diffusion mechanisms can ensure both general grain growth and a coarsening of the $\alpha$ phase. The width of these platelets has been found to range between 3 $\mu m$ and 4 $\mu m$ for the HT1 condition and between 5 $\mu m$ and 8 $\mu m$ for the HT2. The difference between the two heat-treated conditions can be explained by the different treatment temperature of the thermal cycles. HT1 samples are heat treated at a lower temperature in comparison with the HT2 ones. Since the solute diffusion is a direct function of the thermal condition achieved during heat treatment, higher temperatures will correspond to a higher degree of diffusion within the material. This results in a higher movement of solutes from the $\beta$ phase to the $\alpha$ phase which will consequently grow. An increment of the transversal size of the $\alpha$ laths well explains the increment of ductility previously observed. It should also be highlighted that according to previous works, formation of lamellar $\alpha+\beta$ microstructures, including $\alpha$ colonies, results in higher ductility with sacrificing the UCS of the material [50].

4 Conclusions

The effect of the heat treatments on the microstructure and mechanical behaviour of Ti-6Al-4V lattice structures manufactured by EBM was analysed in the present work. In particular, the effect of the unit cell size and unit cell type was investigated for the as-built and heat-treated samples. The main mechanical properties were compared with the Ashby
1. A more homogeneous failure mode, typically more ductile, was found for samples in the heat-treated conditions with respect to the as-built ones. In addition, the barrelling effect was observed in all the samples after the heat treatment.

2. Like the as-built samples, the heat-treated ones did not show a clear effect of the unit cell type and size on their mechanical performance. Nevertheless, the relative density of the structures was the main factor influencing their mechanical behaviour also in the HT1 and HT2 conditions.

3. The heat treatments were able to preserve the stiffness and the compressive strength of the lattice structures. In addition, an increment of both the elongation at failure and the absorbed energy was detected. These increases explain the change in failure mode observed during compression tests.

4. Young’s modulus, UCS and W of the lattice structures in the heat-treated conditions still follow a linear trend in a bi-logarithmic diagram with respect to the relative density.

5. The microstructure of the lattice structures after the heat treatments is still composed by a mix of $\alpha$ and $\beta$ phases. Same microstructural features were observed in the same thermal condition, confirming that the temperature of the heat treatment was the main feature that affects the change of the microstructure of Ti-6Al-4V lattices manufactured by EBM.

6. With respect to the as-built samples, the width of the $\alpha$ platelets in the heat-treated conditions increases. This result well fitted the findings of the mechanical analysis, confirming the increment of ductility due to the HT1 and HT2 conditions with respect to the as-built one.

7. The width of these platelets has been found to range between 3 $\mu$m and 4 $\mu$m for the HT1 condition and between 5 $\mu$m and 8 $\mu$m for the HT2. The difference between the two heat-treated conditions can be explained by the different treatment temperatures of the thermal cycles.

It should be highlighted that in the topology optimization of some complex shape components, a mix of lattice and bulk structures is used to reduce their weight keeping their mechanical performance as high as their fully bulk ones. On the other hand, the heat treatment of bulk parts is highly recommended to improve their mechanical performance. This work clearly exhibited that the recommended heat treatments for the bulk materials can also modify the microstructure of the lattice part and, as a consequence, their mechanical properties.

**Author contribution** M.G. and A.S. conceived and designed the experiment. G.D. performed the characterizations and collected the data. All the authors analysed and interpreted the data. G.D. wrote and revised the manuscript. M.G. and A.S. revised the manuscript and approved the final version to be submitted.
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Availability of data and material The datasets generated during and/or analysed during the current study are available from the corresponding author on reasonable request.

Code availability Not applicable.

Declarations

Ethics approval This chapter does not contain any studies with human participants or animals performed by any of the authors. Authors acknowledge the work is original and all the relevant text from the literature has been properly cited.

Consent to participate Authors agree to the authorship order.

Consent for publication All authors have read and agreed to the published version of the manuscript.

Conflicts of interest The authors declare no competing interests.

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