Photocatalytic, structural and optical properties of mixed anion solid solutions $\text{Ba}_3\text{Sc}_2-x\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2$ and $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2-y\text{Se}_y$†

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Nine members of two contiguous solid solutions, $\text{Ba}_3\text{Sc}_2-x\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2$ and $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2-y\text{Se}_y$ ($x, y = 0, 0.5, 1, 1.5$ and $2$), were synthesised at temperatures between $800$ °C and $900$ °C by stoichiometric combination of binary precursors. Their structures were determined by Rietveld refinement of X-ray powder diffraction data and found to adopt the $\text{SmNi}_2\text{Ge}_2$ structure with $I4/mmm$ symmetry. Approximate Vegard law relationships were found within each solution between the lattice parameters and composition, with an observed cell volume of $466.4$ Å$^3$ for $\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2$ increasing to $481.0$ Å$^3$ for $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2$ and finally to $499.0$ Å$^3$ for $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_2$. In the first solid solution, this volume increase is driven by the replacement of scandium by the larger indium ion, generating increased strain in the copper chalcogenide layer. In the second solution the substitution into the structure of the larger selenium drives further volume expansion, while relieving the strain in the copper chalcogenide layer. Band gaps were estimated from reflectance spectroscopy and these were determined to be $3.3$ eV, $1.8$ eV, and $1.3$ eV for the three end members $\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2$, $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2$, and $\text{Ba}_3\text{Sc}_2\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_2$, respectively. For the intermediate compositions a linear relationship between band gap size and composition was observed, driven in the first solution by the introduction of the more electronegative indium lowering the conduction band minimum and in the second solution by the substitution of the electropositive selenium raising the valance band maximum. Photocatalytic activity was observed in all samples under solar simulated light, based on a dye degradation test, with the exception of $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_1\text{S}_1$. The most active sample was found to be $\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2$, the material with the largest band gap.

Introduction

Layered mixed anion materials have attracted significant attention due to the identification of a number of examples with functional properties such as superconductivity,\textsuperscript{1–4} $p$-type conductivity,\textsuperscript{5–7} and photocatalysis.\textsuperscript{8–11} In these mixed anion materials oxygen is paired with a heavier anion such as sulphur or arsenic, leading to the adoption of structures with alternating layers due to the inability of the larger and more polarisable heavy anions to share crystallographic sites with the oxide anions. In phases where two or more cations are present, the layering is reinforced with separation of the metal ions based on hard–hard or soft–soft interactions leading to a preference to occupy either the oxide layers or heavier anion layers.\textsuperscript{12}

There has been specific interest in the use of oxysulfides, such as $\text{Sm}_3\text{Ti}_2\text{O}_5\text{S}_2$, as visible light photocatalysts for water splitting applications.\textsuperscript{13} The most widely studied metal oxide photocatalysts such as titanium dioxide have wide band gaps in excess of $3$ eV,\textsuperscript{14} which can therefore only be activated by UV light. Interest in metal chalcogenides has been driven by their much smaller band gaps, which would allow more efficient use
of solar radiation, but they have often been found to be unstable due to competing photocorrosion of the sulfide or selenide ions making them unsuitable for use in aqueous environments. The most recent work by Wang et al. has demonstrated overall photocatalytic water splitting from Y\textsubscript{2}Ti\textsubscript{2}O\textsubscript{5}S\textsubscript{2} with IrO\textsubscript{2} and RhCrO\textsubscript{2} co-catalysts and crucially they found this material to be stable with respect to photocorrosion of the sulfide ions. This work further highlights the potential of oxycalogenide materials as visible light responsive photocatalysts, and opens up the possibility of using the structural and compositional diversity of the quinary oxycalogenides to apply materials design to optimise a visible light active photocatalyst.

For a single junction water splitting photocatalyst the band gap is the principal materials criteria for efficacy. The ideal band gap value lies in the range 1.6 eV to 2.5 eV and is a compromise between the need to maximise the solar flux that can be absorbed and the need to drive the water splitting reactions with sufficient over potential. In addition to the principle criteria of band gap, a review by Inoue has identified, based on empirical observation, a number of additional materials criteria required to ensure sufficient kinetics for a viable photocatalyst. The two most important observations are that (1) active photocatalysts typically contain metal ions with d\textsuperscript{9} or d\textsuperscript{10} configurations, and (2) these cations have a distorted or asymmetric co-ordination environment. Inoue postulated that the closed shell configuration is necessary to minimise electron–hole recombination, as ions with d\textsuperscript{1}–d\textsuperscript{8} configurations could act as charge carrier traps. Ions with a d\textsuperscript{10} configuration were also highlighted as being advantageous as materials containing these cations would have conduction bands consisting of highly dispersed s and p orbitals providing high mobility pathways for photoexcited electrons. The apparent requirement for an asymmetric co-ordination environment was explained as producing a localised dipole favouring electron–hole separation.

In this paper, we report the synthesis, structures, optical properties, and photocatalytic activity of two novel solid solutions series comprising nine samples: Ba\textsubscript{3}Sc\textsubscript{2}–xIn\textsubscript{x}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2} and Ba\textsubscript{3}In\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}–xSe\textsubscript{x} \(x = 0, 0.5, 1, 1.5, 2\). We have found that all these materials meet the primary and secondary prerequisite criteria required for effective solar photocatalysis outlined above. To the best of our knowledge all of these are novel, with the exception of the end member Ba\textsubscript{3}Sc\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}, which we have previously reported. These adopt the A\textsubscript{2}B\textsubscript{2}O\textsubscript{5}C\textsubscript{2}X\textsubscript{2} structure, a variant of the SmNi\textsubscript{2}Ge\textsubscript{2} structure type, where A, B and C are cations and X is a heavy anion. These structures can be considered as being composed of an \([A_{2}B_{2}O_{5}]\)\textsuperscript{2–} layer adopting a fragment of the perovskite structure, and a \([C_{2}X_{2}]\)\textsuperscript{2–} layer where the third cation is in tetrahedral co-ordination to the heavy anion, and can be considered as a fragment of the anti-litharge structure. The A\textsubscript{2}B\textsubscript{2}O\textsubscript{5}C\textsubscript{2}X\textsubscript{2} structure has been adopted by materials containing a number of different \([C_{2}X_{2}]\)\textsuperscript{2–} heavy anion layers including copper sulfide, silver selenide, and iron arsenide compounds, and which can be considered as part of a larger family of mixed anion compounds which have previously been reviewed. In these materials, the properties are often dictated by the heavy anion layer. For example, in iron arsenide superconductors the heavy anion layer acts as the charge carrier layer, and similarly in p-type conducting copper sulphides the heavy anion layer is the transport layer.

For the solid solutions Ba\textsubscript{3}Sc\textsubscript{2}–xIn\textsubscript{x}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2} and Ba\textsubscript{3}In\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}–xSe\textsubscript{x} we will show that the band gap can be controlled as a function of composition, spanning the useful range for photocatalysis of 1.32 eV to 3.27 eV. They also contain the d\textsuperscript{10} indium(II) ion in an asymmetric co-ordination environment, which can favour electron–hole separation, while the presence of copper chalcogenide layers are anticipated to act as effective hole conduction pathways. Finally, the photocatalytic ability of the materials under solar simulated radiation has been directly confirmed using a dye degradation test.

**Experimental methods**

**Solid-state synthesis**

Samples in the solid solutions Ba\textsubscript{3}Sc\textsubscript{2}–xIn\textsubscript{x}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2} and Ba\textsubscript{3}In\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}–xSe\textsubscript{x}, with \(x = 0, 0.5, 1, 1.5, 2\) were prepared on a 0.5 g scale by combining appropriate stoichiometric ratios of binary sulfide, selenide and oxide precursors in a nitrogen filled glove box. Samples were pelleted and placed in alumina crucibles, before being sealed under vacuum in silica ampoules. The alumina cubes prevented the samples from contacting the silica tubes with which they could react at elevated temperatures. The sealed pellets of Ba\textsubscript{3}Sc\textsubscript{2}–xIn\textsubscript{x}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2} (series 1) were heated for 12 hours at 800 °C while samples of Ba\textsubscript{3}In\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}–xSe\textsubscript{x} (series 2) were heated for 24 hours at 900 °C. The precursors used were Sc\textsubscript{2}O\textsubscript{3}, In\textsubscript{2}O\textsubscript{3}, Cu\textsubscript{2}O, Ba\textsubscript{2}O\textsubscript{3}, BaS, BaO, and BaSe. Sc\textsubscript{2}O\textsubscript{3} (Sigma-Aldrich, 99.9%), In\textsubscript{2}O\textsubscript{3} (Sigma-Aldrich, 99.99%) Cu\textsubscript{2}O (Sigma-Aldrich, 99.99%) and Cu\textsubscript{2}O (Sigma-Aldrich, 99.9%) were purchased and used as provided. BaS was synthesized by the reaction of BaCO\textsubscript{3} (Alfa Aesar 99.99%) with CS\textsubscript{2} vapour (Fisher, 99.8%) in argon (BOC Pure-shield), at 900 °C for 8 hours. BaO was synthesized by decomposition of BaCO\textsubscript{3} under vacuum at 1000 °C for 14 hours. BaSe was produced in a two-stage process. In the first step, water insoluble barium selenite was prepared by precipitation upon mixing of two 200 ml aqueous solutions; one of 4.3 g of Na\textsubscript{2}Se\textsubscript{4}O\textsubscript{6} (Sigma-Aldrich, BioXtra) and the other of 6.0 g Ba(NO\textsubscript{3})\textsubscript{2} (Sigma-Aldrich, 99%), chilled to 0 °C over ice. This produced a white precipitate of BaSeO\textsubscript{4} that was filtered and dried in air at 70 °C. The BaSeO\textsubscript{4} was then reduced under an atmosphere of 5% H\textsubscript{2} in N\textsubscript{2} (BOC) at 500 °C for 4 hours, to yield BaSe. The purity of all synthesized precursors was confirmed by X-ray diffraction. All precursor storage and handling was carried out in a nitrogen-filled glove box. Once prepared, samples of Ba\textsubscript{3}Sc\textsubscript{2}–xIn\textsubscript{x}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2} and Ba\textsubscript{3}In\textsubscript{2}O\textsubscript{5}Cu\textsubscript{2}S\textsubscript{2}–xSe\textsubscript{x} were found to be air stable and stored under standard atmosphere.

**Materials characterisation**

The layered copper chalcogenide samples were characterised using powder X-ray diffraction patterns collected on a Bruker D2 diffractometer, equipped with a copper K\textsubscript{α} X-ray source. Patterns were collected in the range 10° < 2θ < 100° two theta, with a step size of 0.02° and a collection time of at least 3 hours.
Patterns were analysed by the Rietveld refinement method carried out using the GSAS-II software suite. An additional diffraction pattern was collected on a sample LaBa and this was used as the crystalline standard to provide a pseudo-voigt peak profile function to account for instrumental broadening, and used in each of the subsequent refinements. The compounds were also analysed using EDX spectroscopy, with data collected using a JOEL JSM5910 scanning electron microscope with a 10 kev acceleration voltage, and the Oxford INCA 300 EDS system.

Diffuse reflectance spectra were collected on the powder samples using a Perkin Elmer Lambda 750S spectrometer, equipped with an integrating sphere. Data were collected in the range of 300 nm to 2500 nm, and the Kubelka–Munk relationship used to estimate sample absorption. Band gaps for the samples were determined using the Tauc method from this spectroscopic data.

**Photocatalysis tests**

An assessment was made of the photocatalytic potential of the materials. For this, the samples were decorated with a cobalt oxide co-catalyst, using a procedure modified from the literature. 25 mg of each chalcogenide powder sample was impregnated with 2 ml of a 8.59 × 10⁻⁴ mol dm⁻³ solution of Co(NO₃)₂·6H₂O (Sigma Aldrich, 98+%) in acetone, and then left exposed to air to allow the solvent to evaporate overnight. The resulting powder samples were heated to 700 °C under nitrogen (flow rate: 250 ml min⁻¹) for 60 min, decomposing the cobalt nitrate to presumed metallic cobalt nanoparticles. The active CoOx co-catalyst was obtained on the powder surface by mild oxidation of the cobalt loaded powders in air at 200 °C for 1 h.

The photocatalytic test used was the degradation of a blue dye, dichloroindophenol (DCIP, Acros 98+%), in the presence of a glycerol as a sacrificial oxidant (Fisher, reagent grade). The test solution was made up in dichloromethane (DCM, Fisher, reagent grade) with a concentration of DCIP of 5.5 × 10⁻⁵ mol dm⁻³ and a concentration of glycerol of 5.5 × 10⁻⁴ mol dm⁻³. In each experiment, a 5 mg sample of the cobalt loaded oxychalcogenide powder was placed in the test solution and agitated by a magnetic stirrer. The slurry was exposed to a 5-sun solar simulator (LS0104 150 W Xenon lamp) with a measured intensity of 509 mW cm⁻² for 3 hours, and then a centrifuge was used to separate the powder from the dye solution. The solution was then transferred to a cuvette and a visible absorption spectrum recorded in the range 400 nm to 800 nm, using a PE750S spectrometer. Changes in dye concentration caused by photocatalytic degradation were determined assuming a Beer-Lambert law relationship between absorption and concentration.

**Computational methodology**

Computational calculations were carried out using density functional theory (DFT) within the Vienna *Ab initio* Simulation Package (VASP). The hybrid functional HSE06 (ref. 38) (α = 25%) was used to accurately describe the nature of the electronic structure of each end member compound relative to experiment and has been shown to accurately describe Sr₃Sc₂O₅Cu₂S₂ and Ba₃Sc₂O₅Cu₂S₂ in previous work. To describe the interaction between the core and valence electrons, the projector augmented wave (PAW) method was employed. The computational workflow involved a geometric optimisation of each compound, Ba₃Sc₂O₅Cu₂S₂, Ba₃In₂O₅Cu₂S₂ and Ba₃In₂O₅Cu₂Se₂, using a Γ-centred 6 × 6 × 2 k-point grid and a plane-wave energy cut-off of 500 eV where convergence was deemed complete when the maximum force on any atom was less than 0.01 eV Å⁻¹.

Density of states (DOS), band structure and optical absorption calculations were carried using the relaxed cells and plotted using the open source python package: sumo. The optical absorption spectra were calculated using the real and imaginary parts of the dielectric constant calculated through a Kramers-Kronig transformation and a summation over the unoccupied bands respectively using a method by Furthmuller and coworkers. Within this formalism however, intra-band and indirect absorptions are ignored and only the direct valence to conduction band transitions are considered.

The effective masses of charge carriers (m*ᵢ) can be calculated using the relationship:

$$\frac{1}{m*ᵢ} = \frac{\delta^2 E(k)}{\delta k^2}$$

where E(k) is the eigenvalue of the band at a specific k.

Calculation of the phonon spectra was performed using the finite-displacement method within the Phonopy code using the PBEsol functional (with a + U value of 5.17 eV applied to the copper atoms) known for accurately describing the structural parameters and bond lengths necessary for accurate phonon calculations. Initially each compound was relaxed to a tight electronic convergence criterion of 1 × 10⁻⁸ eV Å⁻¹ and force convergence of 1 × 10⁻³ eV Å⁻¹ such that the residual forces on all the atoms was minimal.

**Results and discussion**

All targeted members of the two solid solutions, Ba₃Sc₂₋ₓInₓO₃Cu₂S₂ (series 1) and Ba₁In₂O₅Cu₂S₂₋ₓSeₓ (series 2), were successfully made with a minimum 95% purity, and an average 97.7% purity as determined by XRD and supported by EDX measurements. The powder X-ray diffraction patterns of the target compounds were refined from a starting model based on the previously reported Sr₃Sc₂O₅Cu₂S₂ structure, but with appropriate ion substitutions to match the assumed composition. In each refinement the background, lattice parameters and atomic positions were refined. Uniaxial size and strain parameters were refined to account for peak broadening beyond the instrumental broadening determined from modelling data collected on a LaBa high crystallinity sample. Constraints were applied to make the thermal ellipsoids of identical atoms equal. The positions of the Sc/In mixed cation sites in series 1 and the S/Se mixed anion sites in series 2 were also constrained to be identical. Initially the isotropic thermal ellipsoid parameters of the atoms were refined, but these were found to be too strongly correlated to the atomic site positions, preventing both from...
being be refined simultaneously while still producing meaningful results. To overcome this, fixed values for the thermal displacement for each atom type were used (for example 0.02 Å² for all barium atoms, full list in ESI Tables S1 and S2†) allowing the atomic site positions to be refined so that meaningful comparisons of bond distances and angles could be made between samples. The values for these fixed thermal displacements were derived by taking the average values from the nine initial refinements. Additional peaks were also observed in each diffraction pattern, which could not be assigned to the main phase. These were due to impurity phases, variously BaCO₃, BaCu₂S₂, and Sc₂O₃. These were modelled using the standard structures from the ICSD and literature, allowing for the phase fractions to be refined. Lattice parameters and particle size broadening parameters were also refined for these impurity phases where sufficient peaks could be observed.

Using this methodology, good fits to the data were found for all models based on the expected compositions, with wR values ranging from 3.16% to 4.55%, confirming the successful formation of the target phases. The diffraction patterns and their model Rietveld fits can be found in the ESI Fig. S1 to S3,† with an example given in Fig. 1 of the refined fit to the diffraction data collected on Ba₃In₂O₅Cu₂S₂. The purity of the samples was found to be high, with the principal phase comprising between 95.6 wt% to 98.7 wt% in each case. A summary of the refinement results for the series 1 samples can be found in Table 1, and the series 2 samples in Table 2. Full details of the structural refinements can be found in the ESI in Tables S1 and S2,† including the refined atomic site positions, thermal ellipsoid values used, and impurity concentrations.

The results of the analysis of the diffraction data were supported by energy dispersive X-ray spectroscopy (EDX). For each sample, EDX data were collected on 5 different particles chosen at random, and the elemental composition quantified based on the expected heavy elements, with oxygen excluded from the analysis due to presence of environmental contaminants containing oxygen preventing reliable estimation of the amount of this element in the sample. The average elemental composition for each sample resulting from this analysis is shown graphically in Fig. 2, alongside the values expected from the targeted stoichiometry as a guide. These show a good match between the experimental and expected values, so that we can conclude that both the XRD and EDX data confirm that the target phases have been made as intended. The end member Ba₃Sc₂O₅Cu₂S₂ has been previously reported, however to the best of our knowledge the solid solution end members Ba₃In₂O₅Cu₂S₂ and Ba₃In₂O₅Cu₂Se₂, alongside all the intermediate phases, are reported in this work for the first time.

Lattice parameters for the layered oxychalcogenides derived from the Rietveld refined structural models, as a function of composition, are displayed in Fig. 3. These show a good approximation to Vegard’s law for both solid solutions. In series 1 the replacement of the smaller scandium ion (radius of 0.75 Å) for the larger indium ion (radius of 0.93 Å) would be expected to result in a reduction in the lattice parameter.

Table 1 Summary Rietveld refinement for series 1 compounds Ba₃Sc₂₋ₓInₓO₅Cu₂S₂. All structures were refined in I4/mmm, and errors are two standard deviations. Full site refinement results and CIF files are available in the ESI. Values of a, c and volume given in italics are the result of the computational modelling based on HSE06 functional.

| Compound | Lattice parameter a/Å | Lattice parameter c/Å | Volume/A³ | Data points | Purity | Parameters | wrp | RF | Chi2 |
|----------|------------------------|------------------------|-----------|-------------|--------|------------|-----|-----|-----|
| Ba₃Sc₂O₅Cu₂S₂ | 4.1458(2) | 27.38 | 466.42(6) | 4444 | 95.6% | 34 | 3.72% | 2.04 |
| Ba₃Sc₁.₉In₀.₁O₅Cu₂S₂ | 4.1377(2) | 27.218(2) | 470.50(5) | 4444 | 96.1% | 29 | 3.43% | 1.98 |
| Ba₃ScInO₅Cu₂S₂ | 4.1680(3) | 27.317(4) | 474.55(8) | 4444 | 98.7% | 24 | 3.99% | 2.38 |
| Ba₃Sc₁.₅In₁.₅O₅Cu₂S₂ | 4.1772(2) | 27.401(2) | 478.12(6) | 4444 | 97.9% | 24 | 3.16% | 1.96 |
| Ba₃In₂O₅Cu₂S₂ | 4.1862(1) | 27.444(1) | 480.95(2) | 4345 | 97.5% | 30 | 4.46% | 1.93 |

Fig. 1 Rietveld refinement of I4/mmm structure of Ba₃In₂O₅Cu₂S₂ to diffraction data, with lattice parameters a = 4.1862 Å and c = 27.444 Å. Upper section: diffraction data is in blue, model is in green and background in red. Inset shows the high angle region from 60° to 100° 2θ. Lower section shows the difference curve (cyan) and tick marks indicating the positions of the peaks of, in descending order: Ba₃In₂O₅Cu₂S₂ (green), BaCu₂S₂ (red) and BaCO₃ (cyan).
with the larger indium ion (0.80 Å) leads to a steady increase in both the \(a\) and \(c\) lattice parameters, with an increase of approximately 1% in both \(a\) and \(c\) once full replacement by indium is achieved. In series 2, where sulphur (1.84 Å) is replaced with selenium (1.98 Å) in \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2\), we observe a similar increase in both \(a\) and \(c\) lattice parameters. Coincidentally, the increase in \(a\) in series 2 occurs at a similar rate as a function of the fraction of substitution as in series 1, although that of the \(c\) parameter is greater. Overall in series 2 there is an increase of 0.9% in \(a\) in series 2 for the full substitution of selenium, but an expansion of approximately 2% in the \(c\) parameter.

The results of the refinement of the atomic site positions within the unit cell models provides bond lengths and angles, and therefore insight into the changes in the structures across the solid solutions that drive the overall expansion of the unit cells. The limitations of laboratory X-ray diffraction equipment mean that the position of the light oxygen atoms can only be ascertained with limited confidence. However, it is still possible to draw conclusions regarding the general trends, and with greater confidence for the heavier atoms. Fig. 4 shows variations in key bond lengths and angles across the structures as a function of composition. These values can be found tabulated in the ESI in Table S3.

### Table 2

Rietveld refinement results for series 2 compounds, \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2\), \(x\). All structures were refined in \(\text{i4} / \text{mmm}\), and errors are two standard deviations. Full site refinement and CIF files are available in the ESI. Values of \(a\), \(c\) and volume given in italics are the result of the computational modelling based on HSE06 functional. *Also the end member of series 1 data repeated her for convenience.

| Compound                  | Lattice Parameter \(a/\text{Å}\) | Lattice Parameter \(c/\text{Å}\) | Volume/\(\text{Å}^3\) | Data Points | Reflections (main phase) | Parameters | Purity (%) | \(WR_p\) (%) | \(RF^2\) (%) | \(\chi^2\) |
|---------------------------|----------------------------------|----------------------------------|------------------------|-------------|--------------------------|------------|------------|--------------|--------------|------------|
| \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2\) | 4.1862(1)                       | 27.444(1)                        | 480.95(2)              | 4345        | 98                       | 23         | 97.5%      | 4.46%        | 3.12%        | 1.93       |
| \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2\text{S}_0.5\text{Se}_{0.5}\) | 4.1958(2)                       | 27.576(2)                        | 485.47(5)              | 4444        | 106                      | 30         | 98.7%      | 4.11%        | 3.87%        | 1.72       |
| \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_{1.5}\text{S}_{0.5}\) | 4.2060(2)                       | 27.716(2)                        | 490.31(5)              | 108         | 8                        | 30         | 98.6%      | 3.85%        | 3.55%        | 1.93       |
| \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_2\text{S}_0.5\text{Se}_{0.5}\) | 4.2138(2)                       | 27.841(2)                        | 494.35(6)              | 98          | 8                        | 30         | 98.5%      | 4.11%        | 3.87%        | 3.50       |

**Fig. 2** Plot of elemental composition as determined by EDX excluding oxygen, for the two solid solutions: \(\text{Ba}_3\text{Sc}_2\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2\text{S}_0.5\text{Se}_{0.5}\). Thin solid lines represent the percentage of each element expected based on the target composition.

**Fig. 3** Plot of lattice parameters for the \(\text{Ba}_3\text{Sc}_2\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{Sc}_2\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2\text{S}_0.5\text{Se}_{0.5}\) solid solutions \((x, y = 0, 0.5, 1, 1.5, 2)\) as a function of composition. The a lattice parameter scale is to the left and values are shown as black squares. The c lattice parameter scale is to the right, and values are shown with hollow triangles. Error bars are smaller than the symbols used, and the dashed lines are guides for the eye, and indicative of the Vegard law relationship between lattice dimensions and composition.

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direction must be matched by an expansion in that direction in the other block in order to maintain a commensurate $a$ lattice parameter. For example, an expansion of the oxide block in the [100] direction due to a substitution would inevitably force a change in the bonding or geometry to the chalcogenide layer even if it remains compositionally unchanged. In contrast changes to the dimensions of a block parallel to the [001] direction can occur independently, without necessarily affecting the structure of the other layer. Thus changes to the structure that lead to changes in the $a$ lattice parameter are dependent upon both oxide and chalcogenide blocks, whereas changes in the $c$ direction can occur due to either variations in the height of the oxide block, the chalcogenide layer, or the interlayer spacing, and these can be independent of each other.

In series 1 there is steady overall increase in the value of both the $a$ and $c$ lattice parameters of approximately 1% from Ba$_3$Sc$_2$O$_5$Cu$_2$S$_2$ to Ba$_3$In$_2$O$_5$Cu$_2$S$_2$. The key structural change is the substitution of the larger indium into the oxide block which drives the 1% expansion of the cell in the $a$ direction. The geometry of the Sc/In site is pyramidal, and the equatorial metal oxygen bond increases in length by ~0.7% across the series, accounting for the majority of the expansion in the $a$ lattice parameter, the rest of the expansion coming from a small change in the geometry with a decrease in the O$_{eq}$–M–O$_{eq}$ [M = Sc/In] bond angle from 97.8(5)$^\circ$ to 96.7(4)$^\circ$ as the average metal site position moves towards the sulfur. The most significant bond length change is the increase in the axial M–O bond length from 1.98(1) Å to 2.062(3) Å, an increase of ~4%. It is this increase which drives the overall expansion of the cell in the $c$ direction. The response of the compositionally constant copper sulphide layer to the expansion in the $a$ lattice parameter is a reduction in the block height parallel to the [001] direction, counter to the overall expansion of the $c$ lattice parameter. As might be expected the Cu–S bond length remains approximately constant, with the change in the height of the copper containing layer instead being driven by a distortion in the copper geometry, observed by the increase in the S–Cu–S angle from 113.7(5)$^\circ$ to ~115.8(4)$^\circ$. Therefore, the decrease in the sulfide block height with expansion in the [001] direction is driven by changes in the oxide block, but the overall size of the unit cell increases in the $c$ direction because of the larger increase in the height of the [Ba$_3$M$_2$O$_5$]$^{2+}$ layer.

This accordion-like scissoring of the copper sulfide block with an inverse relationship between the block height and the $a$ lattice parameter due to distortions in the copper sulfur bond angles follows the trend observed in the oxysulfides, and accounts for the compatibly of the copper chalcogenide layers with a diversity of metal oxide layers of differing dimensions. Prior works on related materials have found examples of copper sulfide layers that can accommodate values of $a$ lattice parameter as low as 3.83 Å in Ca$_4$Fe$_2$O$_6$Cu$_2$S$_2$ and as high as 4.08 Å in Sr$_2$Sc$_2$O$_5$Cu$_2$S$_2$ or up to 4.12 Å if the fluoride layered BaFCuS is considered.50 The values of $a$ lattice parameter we have identified for the Ba$_3$Sc$_2$–In$_2$O$_5$Cu$_2$S$_2$ solid solution of 4.146 Å to 4.186 Å significantly extends the range of feasible dimensions for layered copper sulfides, and to our knowledge are the largest values yet reported. The end member Ba$_3$In$_2$O$_5$Cu$_2$S$_2$ may well be reaching the limit of what is possible for a stable [Cu$_2$S$_2$]$^{2-}$ layer, with a S–Cu–S angle of approximately 116$^\circ$ showing significantly higher distortion away from tetrahedral geometry than any prior example.

In series 2, Ba$_3$In$_2$O$_5$Cu$_2$S$_2$–Se$_x$, the expansion of the lattice parameters is driven by changes in the chalcogenide layer, in contrast to series 1 where it occurs in the oxide layer. With the
substitution of the larger selenium for sulphur we see the expected increase in the copper chalcogenide bond length, of 2.7% across the series. Simultaneously we observe a relaxation of the copper environment back towards a more ideal tetrahedral geometry, with the \(\text{CH–Cu–CH} \) bond angle decreasing to 112.5(1)° indicating that the larger copper selinide layer is a better, less strained match for the \([\text{Ba}_3\text{In}_{2}\text{O}_5]\)^{2+} layer than the copper sulfide layer. The combined effect of these changes is an expansion of the \(a\) lattice parameter of ~0.9%, and also a very significant increase in the height of the chalcogenide block in the \([001]\) direction across the series of 7%. The response of the now compositionally unchanging \([\text{Ba}_3\text{In}_{2}\text{O}_5]\)^{2+} layer to the increase in the \(a\) lattice parameter is a compensatory decrease in height parallel to the \([001]\) direction, although the effect is smaller than the similar compensation effect observed in the chalcogenide layer in series 1. The equatorial \(\text{In–O}\) bond length increases slightly, by 0.5% across the series, while the apical \(\text{In–O}\) length remains approximately constant. The key effect of the changing dimensions of the oxide block is a change in the geometry of the indium ion with the \(\text{O–In–O}\) bond angle decreasing in order to accommodate the increase in the \([100]\) direction, and this is the cause of the overall decrease in the height of the oxide block.

The results of the computational modelling of the structures of the end member compositions using the \(\text{HSE06}\) functional and \(\text{PBEsol}\) functional are provided in the ESI in Tables S4 and S5,† including the lattice parameters, bond lengths and bond angles. Each of the end member compounds displayed the same \(\text{I}4/\text{mmm}\) symmetry after geometric relaxation to within 0.01 Å⁻¹. Each of the calculated lattice parameters are within 2% of the experimental values owing to the efficacy of both \(\text{HSE06}\) and \(\text{PBEsol}\) in describing the structural properties of this family of layered oxychalcogenide.¹⁹,²⁷ As finite temperatures are typically neglected from DFT, these results indicate that there is minimal thermal expansion and change to the structural properties between 0 K and RTP and thus it is unlikely that the calculated electronic properties will deviate from those observed through experiment. As expected, the substitution of \(\text{S}\) for \(\text{Se}\) increases the \(a\) and \(c\) parameters and increases all of the bond lengths respectively whilst the \(\text{Cu–Ch–Cu (Ch = S, Se)}\) bond angle decreases. This results in a contraction of the \([\text{Cu}_{2}\text{Ch}_{2}]^{2-}\) layers shown by the \(\text{Ba–Ba}\) interlayer distances, or ‘block height’ also seen in the experimental values. In terms of bond lengths, the layers typically remain independent, \(i.e.\) between \(\text{Ba}_3\text{Sc}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) the \(\text{Cu–Ch}\) and \(\text{Cu–Cu}\) distances show minimal changes, yet within the \([\text{Ba}_3\text{M}_2\text{O}_5]\)^{2+} layer, the \(\text{Ba–O}\) and \(\text{M–O}\) distances undergo a larger change than between \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{Se}_2\). As mentioned in previous work, the influence of structure as well as composition plays a distinct role in the tunability of these layered oxychalcogenide semiconductors.¹⁹

In order to estimate the band gaps for the materials, diffuse reflection spectra were recorded on each of the powder samples and the reflectance data were modelled using the Kubelka-Munk function, \(f(R)\). Tauc plots of \([f(R)/h\nu]^2\) against photon energy \((h\nu)\) were used to estimate the direct band gap by extrapolation of a tangent from the point of inflection to the abscissa, and can be found in ESI Fig. S4.† This analysis gave band gap values of 3.27(5) eV for \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2\), 1.77(5) eV for \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) and 1.32(5) eV for \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{Se}_2\), the end members of the solid solutions. For the intermediate compositions, there is an approximately linear relationship between the composition and the experimentally determined band gap, as shown in Fig. 5(a), although with a slight deviation for the series 1 solution, \(\text{Ba}_3\text{Se}_2\text{–In}_2\text{O}_5\text{Cu}_2\text{S}_2\).

The band structures of the three end members were computationally modelled, to help understand the changes in band gap, and can be seen in Fig. 5(b)–(d), with the density of states diagrams in Fig. 5(e)–(g). For each compound the valence band maxima (VBM) is composed approximately of 50 : 50 \(\text{Cu}\) 3d : \(\text{Ch}\ p\) states meaning that the \([\text{Cu}_{2}\text{Ch}_{2}]^{2-}\) layer dominates the \(\text{p}\)-type conductivity in these systems and has been noted previously.¹⁹,²⁷ The full break down of states at the VBM and conduction band minimum (CBM) are given in the ESI in Table S6.† The majority of the \(\text{O}\) \(2p\) states lie around ~6 eV to ~2 eV for each compound, owing to the electronegativity of oxygen and the reason why typically in metal oxide photocatalysts such as \(\text{TiO}_2\) the VBM lies deep compared to the redox potentials of water.²⁸ It is expected that a better bulk band alignment will exist for each of these compounds due to the VBM moving towards the vacuum due to the overlap between \(\text{Cu} 3d\) and \(\text{Ch}\ p\).

This has the added effect of increasing dispersion at the VBM giving rise to lower effective masses. For \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2\), \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{Se}_2\) and \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{Se}_2\), the direct fundamental band gaps are modelled as 3.04 eV, 1.37 eV and 1.09 eV respectively and are direct (at \(\Gamma\)) with the exception of \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2\) where the VBM occurs at \(\Gamma\) and the CBM at the \(X\) point. The energy difference between the indirect and direct band gap (at \(\Gamma\)) is <2 meV, however it is well known that this type of behaviour gives rise to enhanced exciton lifetimes such as seen in anatase \(\text{TiO}_2\) or \(\text{BiOX (X = Cl, Br, I)}\) photocatalysts.²⁵,²³ In all three end member compounds there exists two degenerate bands at the VBM resulting in heavy and light hole effective masses. The full results of the effective mass modelling are given in the ESI in Table S7,† however herein the light effective masses will be documented, as the path of least resistance will likely be taken. The hole effective masses in the \([\text{Cu}_{2}\text{Ch}_{2}]^{2-}\) plane can be found at \(\Gamma–N\) and \(\Gamma–Z\) whilst the direction corresponding to the interplanar direction is given by \(\Gamma–X\). The \(\Gamma–X\) direction results in highly flat bands as expected with (light) hole effective masses of ~42 \(m_e\), ~84 \(m_e\) and ~41 \(m_e\) respectively. For \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2\), \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{Se}_2\) the light effective masses in the \(\Gamma–N\) and \(\Gamma–Z\) direction are 0.44 \(m_e\) and 0.65 \(m_e\), 0.38 \(m_e\) and 0.51 \(m_e\), and 0.26 \(m_e\) and 0.36 \(m_e\) respectively. It is clear then, that both the increase in \(\alpha\) lattice parameter as well as the exchange of sulfur for selenium results in a lowering of the valence band effective mass.

The composition of the CBM is largely determined by the \([\text{Ba}_3\text{M}_2\text{O}_5]\)^{2+} layer. In the case of \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{S}_2\) and \(\text{Ba}_3\text{In}_{2}\text{O}_5\text{Cu}_2\text{Se}_2\) the CBM is dominated by \(\text{In}\) 5s states mixed with \(\text{O}\) 2s states with negligible contributions from \(\text{Cu}\) 4s, \(\text{Ch}\) ns states and \(\text{Ba}\) 6s states. This is in contrast with \(\text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2\) where...
scandium states do not play a role and instead the CBM is made up of Ba 5d states mixed with Cu 3s + d and negligible O 2s + p states. The reasoning for this is due to the lower lying In s states compared to the Ba d states which results in lower band gaps despite the larger \( a \) lattice parameter from \( \text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2 \) to \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2 \). The CBM dispersion difference between \( \text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2 \) and the In-containing compounds is distinctly noticeable in the band structures in Fig. 5, whereby the In 5s states form highly dispersive bands with effective masses of 0.95 \( m_e \), 0.21 \( m_e \), and 0.19 \( m_e \) respectively. Parallels can be made with the flagship n-type conducting transparent conducting oxide: \( \text{In}_2\text{O}_3 \) which also show the same low CBM effective masses of \( \sim 0.22 \) \( m_e \). In practice this means that \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2 \) and \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_2 \) will possess high electron mobility which will aid transport of photoexcited electrons to the surface of the material to perform catalysis. The In-based systems may also be bipolar semiconductors, a property which has been shown to exist in delafossite \( \text{Cu}_2\text{O}_2\text{Cu} \). The modelled band structures provide insight into the observed experimental trends in the band gap. In series 1 the change in the composition of the CBM moves it lower in energy towards the valance band with increasing indium content, while the VBM itself remains undisturbed. The other key effect of the exchange of indium for scandium in the first series, as observed in analysis of the X-ray diffraction data, is in the expansion of the lattice parameters and an increase in the Cu–Cu distance. This has been previously shown to lead to a small increase in band gap due to decreased dispersion of the valence and conduction bands under the influence of the Cu–Cu interactions. The effect is expected to be approximately only +0.04 eV for the increase in Cu–Cu distance in the \( \text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2 \) solution, however it may account for the small deviation from trend observed for the latter members of the solution, as shown in the first half of Fig. 5(a). In the second solid solution the exchange of sulphur in \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2 \) leads to a shift in the valance band maximum towards the vacuum and giving an overall decrease in the band gap. The effect across the whole of the solution is a decrease of the band gap by 0.45 eV. This is comparable to similar observed differences in band gap energy for pairs of layered oxochalcogenides where both the oxysulphide and oxyselenide are known, for example, \( \text{Sr}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{Ch}_2 \) with band gaps of 3.10 eV for Ch = S and 2.90 eV when Ch = Se, and \( \text{LaOCuCh} \) with band gaps 3.14 eV (Ch = S) and 2.82 eV (Ch = Se).

The optical absorption coefficients were also simulated and can be found in the ESI in Fig. S5† as a function of photon energy. The optical band gaps for \( \text{Ba}_3\text{Sc}_2\text{O}_5\text{Cu}_2\text{S}_2 \), \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2 \), and \( \text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{Se}_2 \) are calculated to be 3.24 eV, 1.84 eV and 1.48 eV respectively. This corresponds well with those gained in experiment (3.27 eV, 1.77 eV and 1.32 eV respectively). A strong (steep) absorption corresponds to an increased likelihood of photoexcited charge carriers and...
Table 3  Band gap and photocatalytic data for the 9 samples in the solid solutions $\text{Ba}_3\text{Sc}_{2-x}\text{In}_x\text{O}_5\text{Cu}_2\text{S}_2$ and $\text{Ba}_3\text{In}_{2-x}\text{Cu}_2\text{S}_{2-y}\text{Se}_y$. Dye degradation is the percentage of the dye degraded after 3 hours exposure to a solar simulator lamp. Error on DCIP measurements ±2.5%

|                     | $\text{Ba}_3\text{Sc}_{2-x}\text{In}_x\text{Cu}_2\text{S}_2$ | $\text{Ba}_3\text{In}_{2-x}\text{Cu}_2\text{S}_{2-y}\text{Se}_y$ |
|---------------------|-------------------------------------------------------------|-------------------------------------------------------------|
| Band gap/eV         | 3.27(5) 2.80(5) 2.41(5) 2.09(5) 1.77(5) 1.65(5) 1.55(5) 1.44(5) 1.32(5) | 3.27(5) 2.80(5) 2.41(5) 2.09(5) 1.77(5) 1.65(5) 1.55(5) 1.44(5) 1.32(5) |
| DCIP degradation    | 27.0% 22.9% 14.8% 15.4% 14.5% 14.5% 5.9% 3.8% 0.3% 5.5% | 27.0% 22.9% 14.8% 15.4% 14.5% 14.5% 5.9% 3.8% 0.3% 5.5% |

Conclusions

We have demonstrated the synthesis of two new solid solutions, $\text{Ba}_3\text{Sc}_{1.5}\text{In}_{0.5}\text{O}_5\text{Cu}_2\text{S}_2$ and $\text{Ba}_3\text{In}_{2-x}\text{Cu}_2\text{S}_{2-y}\text{Se}_y$, and shown that almost all of these display photocatalytic activity. The shared end member $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2$ has a basal lattice parameter of 4.1861 Å, which is the largest yet reported for a layered oxy-sulfide containing anti-litharge structured copper sulphide layer. This therefore expands the upper range for the use of the $[\text{Cu}_2\text{S}_2]^2$ structural unit when considering a building block approach to materials design.

Spectroscopic analysis has shown that the with the two solid solutions it is possible to select, through appropriate choice of composition, a photocatalytic material with any band gap ranging from 3.30 eV to 1.32 eV. This spans the visible spectrum from the near UV to the near IR, although the driving force behind the change in band gap differs for the two solid solutions. From $\text{Ba}_3\text{Sc}_{1.5}\text{In}_{0.5}\text{Cu}_2\text{S}_2$ to $\text{Ba}_3\text{In}_2\text{O}_5\text{Cu}_2\text{S}_2$ the conduction band minimum decreases, while from $\text{Ba}_3\text{In}_{2-x}\text{Cu}_2\text{S}_{2-y}\text{Se}_y$ to $\text{Ba}_3\text{In}_{2-x}\text{Cu}_2\text{S}_{2-y}\text{Se}_y$ the valence band maximum increases. The ability to tune the band gap and band edge positions through composition in the two solid solutions is a key feature that could be used...
in the future in the optimisation of the absorber in a water splitting photocatalyst system.

Data availability

All data supporting this study are openly available from the University of Southampton repository at DOI: 10.5258/SOTON/D1457.

Conflicts of interest

There are no conflicts of interest.

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