First Principle Study on Atomic Scale Structures of Cathode in Aluminium-ion Battery Using Various van der Waals Corrections

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Abstract. There is still controversy on the atomistic configuration of aluminium-ion batteries (AIB) cathode when using first principle calculation based on density functional theory (DFT). We examined the relevant cathodic structures of Al/graphite battery by employing several van der Waals (vdW) corrections. Among them, DFT-TS method was determined to be a better dispersion correction in correctly rendering structural features already found through experiment investigations. The systematic comparison paved the way to the choice of vdW parameters in first principle calculation of graphitic electrode.

1 Introduction

In recent years, with the increase in energy demand and the rapid development of the electronics industry, there is an urgent need for clean and efficient energy storage equipment to meet the needs of intermittent production and wearable equipment. Currently widely used lithium-ion batteries face bottlenecks due to the scarcity of lithium in the earth's crust and the inherent shortcomings of single-electron discharge characteristics[1], and, meanwhile, other metal anode materials, such as sodium, magnesium, potassium, calcium, and aluminium, are considered potential candidates for electrochemical energy storage devices. Among them, aluminium has unique advantages in cost and efficiency due to its high abundance in the earth's crust and three-electron redox characteristics[2][3]. Based on three electron transfer electrode reaction (Al ↔ Al^{3+} + 3e^-), aluminium metal can provide up to 2980mAh/g gravimetric capacity and 8040mAh/cm^3 volumetric capacity[4]. Since Lin[5] et al. made the breakthrough of Al-ion battery, there have been many controversies about the reaction mechanism on the cathode side. This Al-ion battery used aluminium foil as the anode, three-dimensional graphite foam as the cathode, and [EMIm][Cl] mixed with AlCl_3 as the ionic liquid electrolyte[6]. Due to the structural complexity of graphite, how AlCl_3 clusters interplay with the cathode of the Al/graphite battery seems to be a perplexing problem.

In order to explore the mechanism of AlCl_3 intercalation in graphite cathode of Al/graphite batteries and explain the evolution of the graphite interlayer compounds (GICs)[7] structure after AlCl_3 is intercalated in graphite, Wu[8] et al. first proposed a planar quadrangle configuration of AlCl_3. They adjusted the van der Waals interaction in the system by adjusting the C parameter in Grimme’s DFT-D2 method, so that the optimized original graphite layer spacing (3.353Å) was close to the experimental value (3.356Å). They believe that all van der Waals correction related methods are based on experience, so the standard parameters in Grimme's DFT-D2 method can be changed according to the actual system. However, in the calculation using adjusted DFT-D2 method, the configuration of AlCl_3 in the graphite interlayer compound after optimization is a planar quadrangle geometry.

Jung[9], Bhauriyal[10], Gao[11], Wang[12], Li[13] and other researchers believe that the AlCl_3 inserted into the graphite layer should be a tetrahedral configuration. Jung and others put forward different opinions on the work of Wu and others, and they tested DFT-D2, DFT-D3(zero-damping), DFT-D3(BJ-damping), vdW-DF(revPBE), vdW-DF(optPBE), vdW-DF(optB88), vdW-DF(optB86b), vdW-DF(PW86R) these eight dispersion correction methods are used to describe van der Waals force. During the test, the cut-off energy is set at 400eV. Among them, the DFT-D2 method is poor in describing the graphite layer spacing and the calculated pristine graphite layer spacing is 3.2 Å. And the remaining methods obtain the original graphite layer spacing sufficiently accurate, about 3.25–3.35Å. Especially DFT-D3(zero-damping), vdW-DF(revPBE), vdW-DF(optPBE), vdW-DF2(PW86R) methods, the difference from the experimental value of the layer spacing is less than 0.03Å, and the optimized AlCl_3 tends to tetrahedron configuration, 0.36–0.77eV more stable than planar quadrangle configuration AlCl_3.
2 Calculation details

This work uses a first-principles calculation method based on density functional theory (DFT), calculation using the Vienna ab initio simulation package (VASP) software package. Using projector augmented-wave method (PAW) to describe the interaction between valence electrons and ion reals. In order to describe the exchange-correlation potential, the generalized gradient approximation of Perdew-Burke-Ernzerhof (GGA-PBE) were used. Plane waves energy cut-off optimization result is 600 eV. The Brillouin zone integral uses a Gamma centered 4×4×4 k-point grid. In the process of structural relaxation, the lattice volume and atomic position are fully relaxed until the Hellmann-Feynman force on all atoms is less than 1×10⁻⁵ eV/Å, total energy error is less than 1×10⁻⁶ eV. To describe the van der Waals (VDW) interactions, the Tkatchenko-Scheffler (DFT-TS) method was used.

3 Results and discussion

3.1. Calculation model

We first solved the problem of selecting the van der Waals parameters for calculating the graphite system. The graphite layers are stacked together by van der Waals force. In order to obtain the accurate pristine graphite interlayer spacing, four van der Waals force correction methods, such as DFT-D₂[14], DFT-D₃(zero-damping)[15], DFT-D₃(BJ-damping)[16], DFT-TS[17] were tested, respectively, the data are shown in table 1.

Table 1. Approximate vdW correction methods with optimized graphite interlayer spacings.

| Method          | Plane wave cut-off energy(eV) | d(Å)  |
|-----------------|-------------------------------|-------|
| DFT-D₂          | 600                           | 3.25  |
| DFT-D₃(zero-damping) | 500                           | 3.453 |
| DFT-D₃(BJ-damping)  | 600                           | 3.311 |
| DFT-TS          | 600                           | 3.335 |

The graphite interlayer spacing optimized by the DFT-D₂ method converges when the cut-off energy set at 600 eV, which is 3.250Å, it’s 0.086Å lower compared with experimental value (3.336 Å). The graphite interlayer spacing optimized by the DFT-D₃(zero-damping) method converges when the cut-off energy is set at 500 eV, which is 3.453Å, it’s 0.117Å higher than the experimental value. When we test the DFT-D₃(BJ-damping) method, we found that as the plane wave cut-off energy increases, the graphite interlayer spacing fluctuates in the range of 3.306~3.348Å. Although the graphite interlayer spacing can be optimized to 3.311Å at 600eV, this fluctuation is very detrimental to the accuracy of the calculation results. Therefore, we tested the DFT-TS method. When the cut-off energy is set at 450eV or higher, the graphite interlayer spacing converges near 3.34Å. The difference from the experimental value is about ~0.001Å. So we believe that the DFT-TS method is the best way to describe the van der Waals force between graphene layers. The graphite interlayer spacing after relaxation is 3.335Å, which is approximately equal to the experimental value of 3.336Å at 4.2K[18].

As shown in figure 1, the optimized graphite configuration is periodically extended to a 3×3×1 supercell (with 36 C atoms), which simulates the AB stacked graphite of stage-2, and the stage-n of GIC refers to every other layer of graphene separated by an insert AlCl₄ cluster. The follow-up work was carried out in the graphite interlayer compound of stage-2.

3.2. The geometry of AlCl₄ inserted into GIC

First, to understand which tetrahedral AlCl₄ or planar AlCl₄ is more stable in the electrolyte of Al/graphite battery. We calculated the structure of gas phase AlCl₄ with tetrahedral and planar geometry in the vacuum, respectively, as shown in figure 2. The tetrahedron geometry of AlCl₄ is 0.82eV more stable than planar geometry of AlCl₄. The height of the optimized tetrahedral configuration AlCl₄ is about 2.5Å, and the Al-Cl bond length is 2.15Å. The bond length of Al-Cl in planar configuration AlCl₄ is 2.18Å.  

![Figure 1. 3×3×1 AB stacks graphite supercell configuration.](image1.png)

![Figure 2. The geometry of AlCl₄ inserted into GIC.](image2.png)
Previous studies have shown that the distance between the Cl atom in intercalated AlCl$_4$ and the C atom in graphite should be greater than 3Å. In order to accommodate AlCl$_4$ clusters between graphene layers, the graphite interlayer spacing will inevitably expand. In order to investigate whether AlCl$_4$ tends to tetrahedral configuration or planar configuration between graphene layers, we put a tetrahedral configuration of AlCl$_4$ between graphene layers. We used DFT-D3(zero-damping) and DFT-TS van der Waals force correction method to optimize this structure. There are obvious differences in the configuration after relaxation, the AlCl$_4$ between the graphene layers obviously changes to a planar configuration by using DFT-D3(zero-damping) method, and the graphene interlayer spacing becomes 6.41Å, as shown in figure 3(a). Then by using DFT-TS method, the AlCl$_4$ between the graphene layers still maintains the tetrahedral configuration, and the graphite interlayer spacing increases to 8.71Å, as shown in figure 3(b)(c). In previous research, Wang[19] et al. observed the tetrahedral coordinated Al between graphene layers through X-ray absorption spectra, which is in good agreement with the tetrahedral configuration AlCl$_4$ we calculated. This agreement serves as weighty evidence that the DFT-TS method is more accurate in describing the structure of this GICs. Based on this, we mainly studied two tetrahedral configurations of AlCl$_4$ in graphite intercalation: AlCl$_4$ with a 2-fold rotation symmetry about the direction normal to the graphite basal plane(2FR-shape), as shown in figure 3(b); AlCl$_4$ with a 3-fold rotation symmetry about the direction normal to the graphite basal plane(3FR-shape), as shown in figure 3(c).

In terms of energy, the GIC with planar geometry AlCl$_4$ between the graphite layers is about 2eV higher than GICs with tetrahedral geometry AlCl$_4$ between the graphite layers. For tetrahedral geometry AlCl$_4$, the GIC with 2FR shape AlCl$_4$ is about 0.1eV more stable than the GIC with 3FR shape AlCl$_4$, the structural parameters are shown in table 2.

| Geometry of AlCl$_4$ in GIC | Lattice parameters(Å) | d(Å) | d$^{Al-Cl}$(Å) | $\theta^{Cl-Al-Cl}$(°) | d$^{AlCl4}$(Å) |
|----------------------------|-----------------------|------|----------------|----------------------|----------------|
| planar                     | a=7.382; b=7.393; c=9.735 | 6.412 | 2.169 to 2.224 | 89.99 to 90.01 | -               |
| 2FR                        | a=b=7.375; c=12.06    | 8.714 | 2.155 to 2.158 | 107.5 to 114.32 | 2.366          |
| 3FR                        | a=b=7.376; c=12.481   | 9.131 | 2.156 to 2.16 | 107.91 to 110.86 | 2.841          |
4 Conclusion

Investigation of cathode configuration in Al/graphite batteries is of great significance for development of more capable energy storage system. The DFT-TS method we used to correct the van der Waals force can well describe the graphite interlayer spacing and the GICs structure. Furthermore, we found that the most stable configuration of AlCl$_4$ between graphite layers is 2FR shape.

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