Assessment of Wind Turbine Generators on Reliability of Distribution Network

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Abstract
Wind turbine generators (WTG) is predicted to play a prominent role in the electric power systems of the future. Connection of wind turbine generators to the distribution network increases power sources and therefore increases reliability of distribution network. Assessment of reliability of distribution network connected to wind turbine generators based on two state model yields big errors due to dependence of wind source capacity on wind speed which is a variable value. For more accurate assessment results, the article proposes to utilize multi-stage model of wind source reliability and switch section partitioning based on reliability on distribution network.

Keywords Wind turbine generators · Distribution network · Reliability · Multi stage mode

1 Introduction
The distribution networks (DNs) are responsible for supplying electricity directly to the consumers. Therefore, they are responsible for ensuring the quality of electricity service. Changes in grid configuration, status parameters and equipment status in the DNs directly affect the consumers through changes in power quality and power supply reliability [1]. In terms of power quality, DNs is mainly determined by voltage quality indicator. The most effective voltage regulating components such as transformers, compensators are located in the DNs. In different modes of the load, the DN could modify the configuration to ensure the determined voltage quality. In relation to the power supply reliability, DN plays a crucial role because power outage in DN could directly affect the power shortage on the load. In order to improve the reliability in the DN, several measures could be implemented such as installation of reclosers, isolators, grid reconfiguration, etc.

As a sequence, indicators such as the system average interruption frequency index (SAIFI), customer average interruption frequency index (CAIFI), system average interruption duration index (SAIDI), customer average interruption duration index (CAIDI) are widely used to evaluate the power reliability. Determining the relationship between these indicators and the change in power supply is the first step in introducing the solutions to enhance the power reliability of DNs.

One of the highly accurate methods for power reliability assessment is section partitioning. This method employs partitioning switch to partition the grid into sections with different power reliabilities. It is assumed that failures of the fuses are neglectable, the durations of electricity service interrupted to consumers in the same section are similar. Then, configuration by sections shall be basis for analyzing and calculating the power reliability to consumers. In one DN, it is possible to partition it into several load sections. These load sections could be partitioned by interconnected lines by non-automatic breakers devices such as cut-out fuses, disconnecting switch, load switch which are characterized by the same failure’s causes and frequency [2]. The accuracy of calculating the power reliability depends on the reliability model of the elements in the DN. Normally the elements are modeled under
two states of success and failure associated with two parameters of failure probability and resilience probability. With this model, higher errors may be expected as when modeling with multi-state generators such as Wind Turbine Generator (WTG). Recently, wind power integration to the DN has been increased to improve the power supply capability and reduce the probability of power shortage due to lack of power supply.

However, WTG is characterized by unmanageable output power which is entirely dependent on the wind speed as random variable. Thus, this article proposes to utilize multi-state model of wind source reliability and switch section partitioning based on reliability on distribution network to achieve more accurate results of calculating the yearly duration of power shortage due to failures.

2 Reliability Model

2.1 Reliability Model of Multi-state WTG

2.1.1 Wind Velocity Model

Wind speed varies by locations and time. A common expression of wind velocity randomness is the probability density function model Weibull [3].

\[
f(v) = \frac{k}{c} \left( \frac{v}{c} \right)^{k-1} \exp \left[ -\left( \frac{v}{c} \right)^k \right]
\]

(1)

In which:

\( v \) is wind velocity (m/s); \( k \) is the character index varies with the wind of each region (Fig. 1); \( c \) is the rate index calculated based on the average annual wind speed, calculated over several years, shown in Fig. 2.

Probability distribution function:

\[
F(v) = P(V \leq v) = 1 - \exp \left[ -\left( \frac{v}{c} \right)^k \right]
\]

(2)

In this paper, the distribution of wind speed probabilities is described based on the annual average value \( \mu \) and standard deviation \( \sigma \) [3]. With deviation range \( 10 \sigma \), the distribution will include very low probability values. The distribution is divided into \( N_b \) steps at scale of \( 10 \sigma / N_b \). Step center value \( SW_{bi} (i = 1, ..., N_b) \) is defined in Eq. (3) corresponding to the probability of each step \( P_{bi} (i = 1, ..., N_b) \) is defined in the Eq. (4).

\[
\begin{align*}
SW_{bi} &= \mu + \left( \frac{10\sigma}{N_b} \right) (i - 0.5N_b) & \text{with } N_b \text{ as even number} \\
SW_{bi} &= \mu + \left( \frac{10\sigma}{N_b} \right) [i - 0.5(N_b + 1)] & \text{with } N_b \text{ as odd number}
\end{align*}
\]

(3)

\[
P_{bi} = \frac{N_{bi}}{8760 \cdot N_y}
\]

(4)

where \( N_{bi} \) is the number of wind speed data simulation; \( N_y \) is the number of years of simulation (Fig. 3).
2.1.2 Generating Capacity Model of WTG

Generating capacity of WTG directly depends on wind speed. Typical speed thresholds for each WTG:

- $V_{ci}$: minimum operational wind speed;
- $V_r$: wind speed for starting the turbine reaching the rated power;
- $V_{co}$: maximum wind speed allows turbines to operate (for reasons of safety for turbines when the wind is over speed) (Fig. 4).

For each wind speed value is a generating output value:

\[
\begin{align*}
    P_i &= 0 & 0 \leq SW_{bi} \leq V_{ci} \\
    P_i &= P_r (A + B \cdot SW_{bi} + C \cdot SW_{bi}^2) & V_{ci} \leq SW_{bi} \leq V_r \\
    P_i &= P_r & V_r \leq SW_{bi} \leq V_{co} \\
    P_i &= 0 & V_{co} \leq SW_{bi}
\end{align*}
\]  

Values of $A$, $B$, $C$ are calculated in the following formulas [5]:

\[
\begin{align*}
    A &= \frac{1}{(V_{ci} - V_r)^2} \left[ V_{ci}(V_{ci} + V_r) - 4(V_{ci} V_r) \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 \right] \\
    B &= \frac{1}{(V_{ci} - V_r)^2} \left[ 4(V_{ci} + V_r) \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 - (3V_{ci} + V_r) \right] \\
    C &= \frac{1}{(V_{ci} - V_r)^2} \left[ 2 - 4 \left( \frac{V_{ci} + V_r}{2V_r} \right)^3 \right]
\end{align*}
\]  

2.1.3 Multi-state Model of WTG

For WTG with the generating depends on the change in wind speed, the two-state model is unable to describe all generating states. Therefore, it is required to use a multi-state model in order to accurately depict the actual state of the WTG. Each state is characterized by the state power $P_i$ and the state probability $P_{Bi}$ shown in Fig. 5.

The multiple state model presents many advantages that accurately describe the working status of the WTG changes according to wind speed. However, the model encountered many difficulties when calculating the probability of special states when number of states is high. Therefore, simplified multi-state model was proposed in [6] as in Fig. 6.

\[
\begin{align*}
    P_{B_k} &= \left( \frac{P_{k+1} - P_i}{\Delta P} \right) \cdot P_{B_i} \\
    P_{B_{k+1}} &= \left( \frac{P_i - P_k}{\Delta P} \right) \cdot P_{B_i}
\end{align*}
\]
2.2 Computation of Reliability in Distribution Network

2.2.1 Distribution Network Section Partitioning

During the reliability calculations, complex grids are often partitioned into sections with the same reliability parameters. With the DN having large number of nodes, partitioning DN into sections is necessary so as to simplify reliability computation. Section partitioning by reliability is subject to location of the switch. If the failure of the fuse is assumed to be negligible, the supply of electricity to consumers in the one section is the same. In fact, section partitioning based on automatic switches devices also help improving reliability. In case of failure, sections isolated from the main grid could be offgrid. Distributed generators feeding to these offgrid sections may become main supplier for those sections’ loads.

Determination of isolating location to ensure continuous power supply to the load depends on the correlation between the distributed generator capacity and the loads. For the pro-active generators such as diesel, small hydropower, it is possible to determine the power source. Whereas, determination of isolating location faces many difficulties with distributed generator which generating capacity depends randomly on the wind speed parameter.

The IEEE RBTS 25 node grid model on Fig. 7 [7] is partitioned into five sections with different reliability. In particular, in order to improve reliability of Sects. 2, 3, 4, 5, WTG was integrated. These sections can be isolated from the main grid to operate independently in case of failure through the island conditioning unit such as circuit breaker. In the absence of wind power, the cause of the power failure in each Area i (KV_i) can be a fault on the distribution station (DS) that located on the line connected to KV_i from the main power supply or on KV_i itself. For example, for KV3 on set G4 = {KV1, KV3, KV4, DS}. For every failure of each component of the set G, the power failure duration on KV4 is the duration of repair of the defective part [7].

Then, duration of the power outage is calculated as follows:

\[ T^{ND}_k = \left( \sum_{j \in G} \sum_{i=1}^m \lambda_j \cdot r_i \right) \]  \hspace{1cm} (8)

In which:

- \( T^{ND}_k \) is the duration of off-grid for section k;
- \( \lambda_j \) is failure intensity of element i in element j;
- \( r_i \) is duration of repairing of element i; and
- m is the number of elements in section i.

If every section is consider as smaller system within DNs, each section has SAIDI_k and the whole system has SAIDI_s. The two indexes are associated through the formula (9):

\[ SAIDI_s = \sum_k SAIDI_k \cdot \frac{C_k}{C_s} \]  \hspace{1cm} (9)

In which:

- \( C_k \) is the number of load in section k; \( C_s \): total number of loads in the whole DN.

In fact, duration of power shortage is different with formula (13), because sections have distributed generator and operating off-grid. Thus, it is necessary to include the probability function of off-grid mode as follows:

\[ P^{TG}_k = \sum_{j \in G \cap G_4} \frac{T^{ND}_j}{8760} \]  \hspace{1cm} (10)

Then, total duration of power shortage of section k is calculated as follows:

\[ T^{SH}_k = \sum_{j \in G} \sum_{i=1}^m \lambda_j \cdot r_i \]  \hspace{1cm} (11)

In which:

- \( T^{SH}_k \) is the duration of shortage for section k; and
- m is the number of elements in section i.
2.3 Calculating Power Reliability of Distribution Network

In section a, the probability of operation in off-grid mode has been discussed. However, the success of grid isolation is subject to co-relation between capacity of distributed generators and load capacity at the time of isolation. To calculate the reliability indices, it is necessary to calculate the probability of power shortage, when power shortages occur:

\[ P_{TH}^K = P(S_{WTG} < S_L) = \sum_{i=1}^{n} Pb_i \cdot \frac{\tau_i}{8760} \]  \hspace{1cm} (11)

In which:
- \( S_{WTG} \): capacity of wind power integrated to the section in off-grid mode;  
- \( S_L \): load capacity at the time of grid isolation;  
- \( \tau_i \): is the time of \( S_{WTG} < S_L \) is determined based on extended load curve of the section and capacity \( P_i \) at the state \( i \).

From the formula (10) and (11), probability of power shortage when isolating from the grid for the section in consideration:

\[ P_{TL-\text{OFF}}^K = P_{TL}^K \cdot P_{TH}^K \]  \hspace{1cm} (12)

Sectional reliability is determined:

\[ SAIDI_{WTG}^K = 8760 \cdot P_{TL-\text{OFF}}^K + \sum_{i=1}^{m} \lambda_i \cdot r_i \]

\[ = \left( \sum_{j \in G \cap j \neq k} \sum_{i=1}^{m} \lambda_i \cdot r_i \right) \cdot \sum_{i=1}^{n} Pb_i \cdot \frac{\tau_i}{8760} + \sum_{j=1}^{m} \lambda_i \cdot r_i \]  \hspace{1cm} (13)

Once sectional reliability is determined, system reliability can be identified by formula (9).

3 Case Study

3.1 Network Configuration

See Table 1 here.

| Description                          | \( \lambda \) (time/year) | Duration of repair (h) | Average duration of fail (h/year) |
|--------------------------------------|---------------------------|------------------------|-------------------------------|
| Main distribution station            | -                         | 0.6/100                | 24                            | 0.144                         |
| Circuit breaker                      | -                         | 0.36/100               | 32                            | 0.1152                        |
| Transformer 22/0.4 kV                | 400 kVA                   | 1.5/100                | 10                            | 0.15                          |
| Length of grid at each section       | 3 km                      | 6.5/100 (1/km)         | 5                             | 0.325                         |
| Number of customers at each node     | 80 customers              | -                      | -                             | -                             |

3.2 Wind Power Source

One WTG with parameter given in Table 2.

3.3 Absence of WTG

Based on set in Tables 1, 2, 3, 4, 5, SAIDI index was determined for sections and for system in the absence of WTG. Results are shown in Table 6 (Fig. 8).

| Wind speed (m/s) | h/year | Wind speed (m/s) | h/year |
|------------------|--------|------------------|--------|
| 0÷4              | 1104   | 10÷12            | 1232   |
| 4÷6              | 1355   | 12÷14            | 1124   |
| 6÷8              | 1490   | 14÷25            | 811    |
| 8÷10             | 1572   | 25÷35            | 72     |

| WTG capacity, kW | State probability (Without consideration to failures of WTG) | State probability (consideration to failures of WTG) |
|------------------|------------------------------------------------------------|------------------------------------------------------|
| 0                | 0.1342                                                     | 0.1635                                               |
| 15.71            | 0.1547                                                     | 0.1485                                               |
| 103.29           | 0.1700                                                     | 0.1632                                               |
| 265.91           | 0.1794                                                     | 0.1722                                               |
| 503.57           | 0.1406                                                     | 0.1350                                               |
| 816.27           | 0.1283                                                     | 0.1232                                               |
| 1000             | 0.0926                                                     | 0.0889                                               |
3.4 Considering Integrating WTG

Considering integrating WTG in Table 2 into DN. Calculating SAIDI$_4$, off-grid probability:

\[ p_{T4} = \frac{\sum_{j \in G_{4} \cap j \neq 4} T_{j}^{ND}}{8760} = 4.36 \times 10^{-4} \]

In off-grid mode, power shortage may occur when WTG is unable to meet the demand. Power shortage probability is determined based on time of power shortage expressed in load curve in different states of wind power (Table 7 and Figs. 9, 10). The same process was applied for other sections, the results are shown in Table 8.

\[ SAIDI_{4}^{WT} = 8760 \cdot p_{T4}^{WT} \cdot p_{TH}^{WT} + \sum_{i=1}^{m} \lambda_{i} \cdot r_{i} = 4.9041 \ \text{h/year} \]

The calculation results in Table 8 and Fig. 11 indicate that:

- The average System Average Interruption Duration of DN with WTG integrated is substantially improved compared to the case of DN without WTG integrated, especially in sections directly connected to the WTG.
- The similar results are also found in the offgrid mode, when the WTG capacity increases, the probability of power loss and power loss time decreases. When capacity of wind power is significant enough compared to total load capacity in the DN, the power supply reliability has been significantly improved.
- Section partitioning contributes to improve accuracy of power reliability assessment. The power reliability model of multi-state WTG facilitate the consideration of randomness of wind power and load characteristics explicitly.

### 4 Conclusion

Determining the power reliability of DN integrating wind power is a complex problem. When considering this, it is necessary to take into account influencing factors, especially DN configurations, randomness of wind speed affecting WTG generating capacity and load characteristics. For wind power, the traditional reliability model is
no longer suitable because it is unable to stimulate states of WTG. The multi-state model should be used for this purpose. This study has employed a multi-state model of wind power to calculate several reliability indexes considering the characteristics of the sectional load. In this paper, we have not considered in the case of DN integrated by multiple distributed power sources with different generating capacity characteristics. However, it is probable that the proposed method is capable to investigate such problems.

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