Collider signatures of goldstini in gauge mediation

Riccardo Argurio\textsuperscript{1,5}, Karen De Causmaecker\textsuperscript{2,5}, Gabriele Ferretti\textsuperscript{3}
Alberto Mariotti\textsuperscript{2,5}, Kentarou Mawatari\textsuperscript{2,5}, and Yoshitaro Takaesu\textsuperscript{4}

\textsuperscript{1} Physique Théorique et Mathématique
Université Libre de Bruxelles, C.P. 231, 1050 Bruxelles, Belgium

\textsuperscript{2} Theoretische Natuurkunde and IIHE/ELEM
Vrije Universiteit Brussel, Pleinlaan 2, 1050 Brussels, Belgium

\textsuperscript{3} Department of Fundamental Physics
Chalmers University of Technology, 412 96 Göteborg, Sweden

\textsuperscript{4} KEK Theory Center, and Sokendai, Tsukuba 305-0801, Japan

\textsuperscript{5} International Solvay Institutes, Brussels, Belgium

Abstract

We investigate the collider signatures of the multiple goldstini scenario in the framework of gauge mediation. This class of models is characterized by a visible sector (e.g. the MSSM or any extension) coupled by gauge interactions to more than one SUSY breaking sector. The spectrum consists of a light gravitino LSP, behaving as a goldstino, and a number of neutral fermions (the pseudo-goldstini) with a mass between that of the LSP and that of the lightest particle of the observable sector (LOSP). We consider the two situations where the LOSP is either a gaugino-like neutralino or a stau and we assume only one pseudo-goldstino of a mass of $\mathcal{O}(100)$ GeV. The coupling of the LOSP to the pseudo-goldstino can be enhanced with respect to those of the gravitino giving rise to characteristic signatures. We show that the decay modes of the LOSP into a SM particle and a pseudo-goldstino can be significant. For both LOSP scenarios we analyze (pseudo)-goldstini production at colliders. Compared to standard gauge mediation the final state spectrum is softer and more structured.
1 Introduction

In the coming years we will receive the final verdict from the LHC experiments as to whether
low energy supersymmetry (SUSY) is present or not in nature. So far, both ATLAS and CMS
experiments have not seen any signal and imposed strong bounds on the masses of colored
superpartners [1, 2, 3].

In this paper we will work in the general framework of gauge mediation, where the SUSY
breaking effects are communicated to the observable sector by gauge interactions and gravity
effects are subleading. A subclass of these models, namely those with a light neutralino and a
low SUSY breaking scale, has already been constrained by the search for prompt photons plus
missing energy [4, 5, 6, 7, 8]. Given that the most straightforward searches have not yielded
results, it is important at this stage to consider broadening the class of models to assure that
we are not missing anything.

In all generality, in a SUSY model based on gauge mediation the Lightest SUSY Particle
(LSP) is the gravitino (we consider models preserving R-parity). The characteristic signatures
of the model are then driven by the nature of the Lightest Observable-sector SUSY Parti-
cle (LOSP) and by its decay properties. The two most common scenarios are those with a
neutralino or a stau LOSP.

Even within this general framework, it is important to keep exploring less conventional
avenues to make sure that we get the most out of the current searches. One of the motivations
for our work is to explore the theoretical aspects and experimental signatures of the goldstini
scenario [9, 10] (see also [11] for previous work and [12, 13, 14, 15, 16, 17, 18] for follow up
work), in the context of gauge mediation as previously considered in [19].

This scenario arises when there are more than one SUSY breaking hidden sectors interacting
with the observable sector via gauge interactions. Each sector gives rise to a goldstino, a linear
combination of which is eaten by the gravitino while the remaining fields give rise to light,
neutral, spin one-half particles, the pseudo-goldstini. For simplicity, in the following we are
going to consider a set up where there are only two decoupled hidden sectors and hence only
one pseudo-goldstino, but the analysis is trivially extended to the more general case and the
qualitative features of the model are unchanged.

It was shown in [19] that the pseudo-goldstino acquires a mass in the range 1–100 GeV from
radiative corrections, while all supergravity effects can be neglected. If this mass is lower than
that of the LOSP, the pseudo-goldstino becomes the Next-to-Lightest SUSY Particle (NLSP).
In this case one may face situations where the SUSY breaking scale is low, and thus the gravitino is an almost massless LSP, behaving as the massless true goldstino (denoted by \( G \)) up to a very good level of accuracy. Yet, the LOSP decays predominantly through other channels, namely those containing a massive pseudo-goldstino (denoted by \( G' \)). One of the consequences of this fact is that it softens the spectra of the final states, and we investigate those effects for the two most likely situations where the LOSP is either a gaugino-like neutralino or a stau.

In the case of a neutralino LOSP (denoted by \( \chi \)) the most accessible signature arises when \( \chi \) is mostly a gaugino, promptly decaying into a photon and a (pseudo)-goldstino. The final state will contain photons and missing energy. A mostly gaugino \( \chi \) can also decay into a \( Z \) boson and we will analyze these two situations in detail. It would also be interesting to consider the case where the \( \chi \) has a large higgsino component enhancing its decay into a higgs.\(^1\) For a single sector this was considered in [20], (see also the recent work [21] where mono-photon signals arise directly for higgs decay). In the case of the stau LOSP (denoted by \( \tilde{\tau} \)), the lepton number conservation requires a stau to be created in pairs and the final state contains two taus and missing energy.

Our analysis is independent from many detailed features of the spectrum of superpartners, in the spirit of simplified models. When forced to pick specific values for sparticle masses and mixing angles we will choose those used in common benchmark points [22] such as SPS8 (\( \chi \) LOSP) and SPS7 (\( \tilde{\tau} \) LOSP), in order to make a comparison with the standard gauge mediated models. Other LOSP scenarios, e.g. higgsino-like neutralino LOSP or colored LOSP suggested by general gauge mediation [23], are also interesting to be applied within the goldstini framework and will be reported elsewhere. It should also be emphasized that although the points based on a minimal GMSB model have been constrained by the Tevatron [24] [25] and by the LHC [8], the multiple goldstini scenario eases the constraints due to the softer final spectrum.

We will refrain from considering cosmological issues, just assuming a long enough lifetime for the pseudo-goldstino such that it safely escapes the detector (see e.g. [14] [19] for considerations on the lifetime appropriate to our set up).

The paper is organized as follows: Section 2 provides the theoretical background needed to describe the processes of interest. We discuss the spectrum and the couplings of the pseudo-goldstini to the Supersymmetric Standard Model (SSM). We mainly emphasize the differences from the well known couplings of the true goldstino with SSM fields. As already mentioned above, in the many-goldstini scenario, there are additional particles with masses in between

\(^1\)Shorthand for Brout-Englert-Higgs scalar.
the LOSP and the LSP, the pseudo-goldstini. They come from other hidden sectors, but have
couplings with SSM particles dictated by their nature of being goldstini in each hidden sector.
The pseudo-goldstino has an interaction Lagrangian with the visible sector similar in structure
to the one of the true goldstino, with however couplings that are no longer fixed in terms of
the SSM parameters and the (overall) SUSY breaking scale $F$, but are essentially additional
parameters. They can be computed in a specific set up, but can also be considered free as far
as phenomenological models are concerned. They can easily be enhanced with respect to the
goldstino couplings. Given that this is the most original feature of these models, we focus our
interest on analyzing the dependence of the experimental signatures on these parameters and
on the mass of the pseudo-goldstino for some appropriately chosen simplified spectrum for the
observable sector.

In section 3 we discuss the case of neutralino LOSP. We exemplify some of the features
of these models by first considering processes that do not involve the intricacies of strong
dynamics and can be treated analytically to a large extent. We first study the possible decays
of the neutralino into $(\gamma G)$, $(\gamma G')$, $(ZG)$ and $(ZG')$ pairs. (As mentioned before, in this paper
we restrict our attention to a mostly gaugino $\chi$, and do not consider its decays into a higgs.)
We then compute the production of neutralino and pseudo-goldstino in electron-positron collision
($e^+ e^- \to \chi G'$), which leads to the $\gamma + E_T$ signature. The analytic result for the cross section has
been used to test our FeynRules implementation but it is also of interest in future $e^+ e^-$ linear
colliders such as the ILC. We then simulate the neutralino-pair production, $e^+ e^- \to \chi \chi$, which
gives the $\gamma \gamma + E_T$ signal, also of interest for the ILC.

We compare how the total and differential cross sections change in magnitude and shape
with respect to the standard results obtained in a single goldstino scenario. In particular, the
total cross section of the single photon processes can be enhanced considerably for a pseudo-
goldstino since the couplings of the latter are no longer strictly tied to the overall SUSY breaking
scale. Furthermore, the mass and the coupling of the pseudo-goldstino alters the shape of the
differential cross sections with respect to those of a nearly massless goldstino/gravitino, giving
rise to a softer and more structured spectrum for the photons.

We then proceed to the simulation for $pp$ collisions of relevance to the LHC. We focus on the
following exclusive processes without jets. First we discuss the photon(s) plus missing energy
signals. As a more promising channel, the $l^+ l^- + \gamma \gamma + E_T$ signature is studied in detail, which
is provided by pair production of sleptons, subsequently decaying to a lepton and a neutralino
LOSP. While the total cross-sections are independent from the masses and couplings of the
pseudo-goldstino, the distributions of emitted photons and missing transverse energy do depend
on these parameters and we illustrate this point by simulating various examples.

In section 4 we discuss the case of stau LOSP. We first study the decay widths and branching
ratios of the stau to \((\tau G)\) and \((\tau G')\). We then consider stau pair production in \(pp\) collisions,
studying the \(\tau^+\tau^- + E_T\) signature. There is large SM background, but a satisfactory significance
can be achieved by imposing some kinematical cuts. We find again that the pseudo-goldstino
alters the shape of the differential cross sections with respect to the ordinary gauge mediated
scenario.

We briefly conclude in section 5.

2 The two-sector model and goldstini couplings

2.1 General formalism

The purpose of this section is to derive the relevant couplings of the (pseudo)-goldstino. We
consider a set up where there are two completely decoupled hidden sectors, each communicating
to the SSM through gauge interactions. In other words, each sector is a model of gauge
mediation on its own. (For a review of gauge mediation see [26].) Each sector will then have
a goldstino, \(G_1\) and \(G_2\) respectively, coupling to the SSM particles in a way dictated by the
universal low-energy effective action of the goldstino, applied to each sector. If \(F_1\) and \(F_2\) are
the respective SUSY breaking scales of each sector, and \(F = \sqrt{F_1^2 + F_2^2}\), then the true and
pseudo-goldstino are given by

\[
G = \frac{1}{F} (F_1 G_1 + F_2 G_2),
\]

(1)

\[
G' = \frac{1}{F} (-F_2 G_1 + F_1 G_2).
\]

(2)

For definiteness, we will always assume \(F_1 > F_2\). It has been shown in [19] that, while \(G\) can be
considered massless to all effects, \(G'\) acquires radiatively a mass that is of the order of GeV if
the scales in the two hidden sectors are of the same order. Moreover, when there is a hierarchy
in the SUSY breaking scales \(F_1 \gg F_2\), the mass is enhanced to

\[
m_{G'} \sim \frac{F_1}{F_2} \text{GeV}.
\]

(3)

Since the exact expression for \(m_{G'}\) is very much model dependent, for phenomenological pur-
poses it should be taken as a free parameter, recalling that it will reasonably fall in the 1–100
GeV range. We will always assume that $G'$ is the NLSP, i.e. it is lighter than the LOSP otherwise its presence is virtually impossible to detect.

The couplings of $G$ and $G'$ to the SSM particles can be derived by considering the couplings of $G_1$ and $G_2$, each as if it were the only source of SUSY breaking.

The physical processes we are interested in involve only vertices with at most one (pseudo)-goldstino so we will not have to deal with the intricacies of the full (pseudo)-goldstino Lagrangian. We start by considering the couplings to a generic observable sector whose chiral and vector multiplets we denote by $\Phi \ni (\phi, \psi_\alpha, F_\phi)$ and $W_\alpha \ni (\lambda_\alpha, A_\mu, D)$ respectively (gauge and flavor indices suppressed). After discussing the general features in this language, we present the explicit couplings in the context of the SSM, which are slightly more involved due to the additional presence of Electro-Weak Symmetry Breaking (EWSB).

Let us begin by considering the true goldstino $G$, whose coupling at the linear level is fully understood since the seminal work of the ’70s [27]. It is well known that there are two equivalent ways of writing the linear coupling of $G$ to the matter fields. One is the derivative coupling to the supercurrent $L_{\partial} = \frac{1}{F} (\partial_\mu G^\alpha J^\mu_\alpha + \text{h.c.})$, (4)

where, in the conventions of [28]

$$J^\mu = \sigma^\nu \bar{\psi} D_\nu \phi^\alpha - i \sigma^\nu \bar{\psi} F_\phi + i \frac{1}{2\sqrt{2}} \sigma^\nu \bar{\sigma}^\rho \sigma^\mu \lambda F_{\nu \rho} + \frac{1}{\sqrt{2}} \sigma^\mu \bar{\lambda} D.$$ (5)

The other action is the non-derivative coupling obtained from the previous one by integrating by parts and using the equation of motion to obtain $\Delta_\alpha = \partial_\mu J^\mu_\alpha|_{\text{e.o.m.}}$

$$L_{\partial} = -\frac{1}{F} (G^\alpha \Delta_\alpha + \text{h.c.}).$$ (6)

Since the non-conservation of the supercurrent is entirely due to the presence of supersymmetry breaking soft terms, the expression for $\Delta_\alpha$ must be a function of the latter.

Let us consider the most general soft SUSY breaking terms, namely:

$$L_{\text{soft}} = -\frac{1}{2} m_\lambda \lambda \lambda - \frac{1}{2} m^*_\lambda \bar{\lambda} \bar{\lambda} - U(\phi, \phi^*),$$ (7)

where $U$ is a (at most cubic) gauge invariant function of the scalars, containing for instance the sfermion soft masses and the $B_\mu$ term and $m_\lambda$ are the Majorana masses for the gauginos. The divergence of the supercurrent is now

$$\partial_\mu J^\mu_\alpha = \Delta_\alpha = \frac{m_\lambda}{2\sqrt{2}} \sigma^\mu \bar{\sigma}^\rho \lambda_\alpha F_{\mu \rho} - i \frac{m_\lambda}{\sqrt{2}} \lambda_\alpha D - \psi_\alpha \frac{\partial U}{\partial \phi}.$$ (8)
from which the coupling follows using (6). This expression is valid regardless of whether the
gauge symmetry is spontaneously broken or not (see for instance [29] for a complete treatment
in the MSSM). The form of (6) can also easily be derived from a superspace formulation of
the broken SUSY theory, in terms of the goldstino superfield \( X \).

The derivative and non-derivative actions are completely equivalent, of course, but some
issues are easier to investigate in one formalism than in the other.

It turns out that it is the non-derivative action that is more directly generalized to the
pseudo-goldstino case. This can be seen in various ways but perhaps the easiest argument
comes by looking at the leading high energy behavior of the \( 2 \to 2 \) scattering amplitudes
involving a goldstino. The action (4) contains terms of dimension six and one would expect
the tree-level unpolarized squared amplitudes to scale like \( s^2 \) where \( \sqrt{s} \) is the center of mass
energy. This is not what happens however since SUSY ensures that the leading order behavior
cancels between the different contributions. This must be so since (4) is equivalent to (6) which
contains terms of dimension at most five and yields a scaling of order \( s \).

The same scaling must occur for the pseudo-goldstino since, after all, at tree level it is
a linear combination of two decoupled goldstini, but now the relative coefficients between the
various terms in the action are no longer fixed by SUSY. Using the non-derivative action ensures
that the high energy behavior is preserved. One can of course use the equations of motion
“backwards” and rewrite the non-derivative action in terms of the same type of terms that
appear in the derivative action but with different relative coefficients. In the process however
one also picks up dimension six contact terms schematically like \( G\lambda\psi\psi \) that once again cancel
the \( s^2 \) behavior. Thus it is clearly more convenient to work with (6).

In order to derive the couplings of the pseudo-goldstino, let us start at tree level with the
two fields \( G_h \) (\( h = 1, 2 \)) that are the goldstini of the respective hidden sectors contained in the
superfields \( X_h \). For each goldstino-gaugino-gauge boson vertex, we have

\[
\frac{1}{2} \int d^2 \theta \frac{m_{\lambda(h)} F_h}{F_h} X_h W^2 \supset \frac{m_{\lambda(h)} F_h}{2\sqrt{2} F_h} \lambda \sigma^\mu \sigma^\nu G_h F_{\mu\nu}.
\]  

(9)

For the goldstino-fermion-sfermion vertex, we have

\[
\int d^4 \theta \frac{m_{\phi(h)}^2 F_h^2}{F_h^2} X_h X_h^\dagger \Phi \Phi^\dagger \supset \frac{m_{\phi(h)}^2 F_h}{F_h} G_h \psi \psi^*.
\]  

(10)

The terms (9) and (10) correspond to the first and last terms in (8) inserted into (6), the last
one with \( U = m_{\phi(h)}^2 \phi^* \phi \). We ignore further vertices that do not contribute to the processes of
interest but a full treatment can be found in [30].
Rotating to the $G, G'$ basis, we obtain the couplings

$$\frac{m_\lambda}{2\sqrt{2}F} \lambda \sigma^\mu \bar{\sigma}^\nu GF_{\mu\nu} + K_\lambda \frac{m_\lambda}{2\sqrt{2}F} \lambda \sigma^\mu \bar{\sigma}^\nu G' F_{\mu\nu}$$

(11)

and

$$\frac{m_\phi^2}{F} G\phi^* + K_\phi \frac{m_\phi^2}{F} G' \phi^*,$$

(12)

where $m_\lambda = m_{\lambda(1)} + m_{\lambda(2)}$ and $m_\phi^2 = m_{\phi(1)}^2 + m_{\phi(2)}^2$, and the factors $K_\lambda$ and $K_\phi$ are the ratios between the coupling of the pseudo-goldstino to the one of the true goldstino. Their expressions are

$$K_\lambda = -\frac{m_{\lambda(1)}}{m_\lambda} \frac{F_2}{F_1} + \frac{m_{\lambda(2)}}{m_\lambda} \frac{F_1}{F_2},$$

(13)

$$K_\phi = -\frac{m_{\phi(1)}^2}{m_\phi^2} \frac{F_2}{F_1} + \frac{m_{\phi(2)}^2}{m_\phi^2} \frac{F_1}{F_2},$$

(14)

where in general there will be different coefficients for each gauge group and matter multiplet. In some specific models, there can be relations or bounds between $K_\lambda$ and $K_\phi$. However, in the phenomenological set up, one assumes that these two parameters are free. In any case, below we will use couplings of $G'$ only to a very limited set of (s)particles. The interesting case will be when $K_\lambda, K_\phi \gg 1$. Note however that both cannot be larger than $F_1/F_2$, hence they are limited to be somewhat smaller than $10^3$. (If $F_1/F_2$ is too large, the above picture is no longer valid because the SUSY breaking vacuum of the second sector is destabilized.

2.2 Pseudo-goldstino couplings in the SSM

We now specialize to the case where the observable sector is a SUSY extension of the SM. A couple of technical issues arise since one must also rotate to the physical bases of mass eigenstates of the observable sector after EWSB. More generally the (pseudo)-goldstini will also mix with the particles in the observable sector carrying the same quantum numbers but it is possible to treat this mixing to first order in the SUSY breaking parameter.

Let us begin with the coupling of the neutralino to the $G/G'$ and the photon. This involves an element of the neutralino mixing matrix, essentially proportional to how much the neutralino is the would-be photino. More precisely for the goldstino there is a factor (see e.g. [28])

$$a_\gamma = N_{11}^* \cos \theta_W + N_{12}^* \sin \theta_W,$$

(15)
where $N_{11}^*$ and $N_{12}^*$ are the mixing angles between the lightest neutralino and the Bino and Wino respectively. For the pseudo-goldstino, we can multiply the above by a factor $K_\gamma$ that can be larger than one as discussed above. The relevant part of the Lagrangian is thus

$$\mathcal{L}_{\chi G_\gamma} + \mathcal{L}_{\chi G'\gamma} = \frac{a_\gamma m_\chi}{2\sqrt{2}F} \chi \sigma^{\mu} \bar{\sigma}^{\nu} G_{\mu\nu} + \frac{K_\gamma a_\gamma m_\chi}{2\sqrt{2}F} \chi \sigma^{\mu} \bar{\sigma}^{\nu} G'_{\mu\nu}. \quad (16)$$

The coupling of the goldstino and the pseudo-goldstino to the neutralino and the $Z$ boson is slightly more subtle. Standard computations, such as in [31], use the goldstino couplings in derivative form. After EWSB, there are two such couplings:

$$\mathcal{L}_\partial = i \frac{a_{ZT}}{2\sqrt{2}F} \bar{\chi} \sigma^{\mu} \bar{\sigma}^{\nu} \partial_{\mu} G F_{\nu\rho} - \frac{a_{ZL} m_Z}{\sqrt{2}F} \chi \sigma^{\mu} \bar{\sigma}^{\nu} \partial_{\mu} G Z_{\nu} + \text{h.c.}, \quad (17)$$

where

$$a_{ZT} = -N_{11}^* \sin \theta_W + N_{12}^* \cos \theta_W, \quad (18)$$

$$a_{ZL} = N_{13}^* \cos \beta - N_{14}^* \sin \beta. \quad (19)$$

$N_{13}^*$ and $N_{14}^*$ are the higgsino components of the lightest neutralino, and $\tan \beta$ is the ratio of the vacuum expectation values of the two higgs doublets. The notation follows from the notable fact that the first and second term respectively couple only transverse and longitudinal components of the $Z$ to a massless goldstino.

Integrating by parts and using the equations of motion, one obtains the following terms in the non-derivative Lagrangian:

$$\mathcal{L}_{\chi Z} = \frac{a_{ZT} m_\chi + a_{ZL} m_Z}{2\sqrt{2}F} \chi \sigma^{\mu} \bar{\sigma}^{\nu} G_{\mu\nu} + \frac{m_Z (a_{ZT} m_Z + a_{ZL} m_\chi)}{\sqrt{2}F} \bar{\chi} \sigma^{\mu} G Z_{\mu} + \text{h.c.} \quad (20)$$

It might seem at first that the second term in the Lagrangian above cannot be reproduced using (8). This term appears because after EWSB there are off-diagonal mass terms involving the goldstino and the neutralinos. The mass eigenstates have then to be shifted by $O(1/F)$ terms mixing the goldstino with the neutralinos. Eventually the term above arises from the neutralino gauge couplings, and its precise form follows from using the equations leading to the EWSB vacuum (for a discussion, also including the pseudo-goldstino, see [16]).

The pseudo-goldstino couplings to the $Z$ boson will be of the form above, with however some model dependent factors in front of each term. Since there are two independent terms in
there will be two independent coefficients and we choose to associate them directly to the rescaling of the $a_Z$ and $a_L$ coefficients.\footnote{One could have also chosen to rescale each Lorentz invariant term in \cite{20} independently but this would obscure the comparison in the simulation.}

\begin{align}
\mathcal{L}_{\chi G'Z} &= \frac{K_{ZT} a_{ZT} m_{\chi} + K_{ZL} a_{ZL} m_Z}{2\sqrt{2} F} \chi \sigma^{\mu} \sigma^{\nu} G' F_{\mu\nu} \\
&\quad + \frac{i m_Z (K_{ZT} a_{ZT} m_{\chi} + K_{ZL} a_{ZL} m_Z)}{\sqrt{2} F} \bar{\chi} \sigma^{\mu} G' Z_{\mu} + \text{h.c.} \quad (21)
\end{align}

We now move on to the couplings of the stau. Even in this case the general formula \cite{12} requires some well known modifications after EWSB. Namely, the presence of a SUSY contribution to the tau mass makes the coefficient in the action depend on the difference of the masses in the multiplet. The large soft off-diagonal corrections to the stau mass matrix require rotating from the gauge eigenbasis $\tilde{\tau}_L, \tilde{\tau}_R$ to the mass eigenbasis $\tilde{\tau}, \tilde{\tau}'$. For the couplings to the first two families these effects can be neglected. We focus only on the LOSP $\tilde{\tau} = \cos \theta_{\tilde{\tau}} \tilde{\tau}_L + \sin \theta_{\tilde{\tau}} \tilde{\tau}_R$ and write the Lagrangian as

\begin{align}
\mathcal{L}_{\tilde{\tau} G\tau} + \mathcal{L}_{\tilde{\tau} G'\tau} &= \frac{m_{\tilde{\tau}}^2 - m_{\tilde{\tau}}^2}{F} (\cos \theta_{\tilde{\tau}} G_{\tau L} + \sin \theta_{\tilde{\tau}} G'_{\tau R}) \tilde{\tau}^* \\
&\quad + \frac{m_{\tilde{\tau}}^2 - m_{\tilde{\tau}}^2}{F} (K_{\tau L} \cos \theta_{\tilde{\tau}} G'_{\tau L} + K_{\tau R} \sin \theta_{\tilde{\tau}} G'_{\tau R}) \tilde{\tau}^* + \text{h.c.}, \quad (22)
\end{align}

where we have set $P_{L/R} \tilde{\tau} = \tau_{L/R}$. Once again, we treat the coefficients $K_{\tau L}$ and $K_{\tau R}$ as free parameters.

### 3 The case of the neutralino LOSP

We begin our analysis by considering the case where the neutralino $\chi$ is the LOSP. For this we use the Lagrangians \cite{16, 20} and \cite{21}.

#### 3.1 Decays of the neutralino

The partial widths for neutralino decay into a photon and a (pseudo)-goldstino are:

\begin{align}
\Gamma(\chi \rightarrow \gamma G) &= \frac{a_{\gamma}' m_{\chi}^5}{16 \pi F^2}, \quad (23) \\
\Gamma(\chi \rightarrow \gamma G') &= \frac{K_{\gamma}^2 a_{\gamma}' m_{\chi}^5}{16 \pi F^2} \left( 1 - \frac{m_{G'}^2}{m_{\chi}^2} \right)^3. \quad (24)
\end{align}
We could also write $F = \sqrt{3}m_{3/2}M_p$ in the denominators above, with the mass of the gravitino (i.e. the true goldstino) $m_{3/2}$ and the reduced Planck mass $M_p = 2.43 \times 10^{18}$ GeV.

For a rather massive pseudo-goldstino, the factor between parenthesis can be significantly smaller than 1, though it is always of $\mathcal{O}(1)$ barring any fine tuning of $m_{G'}$ against $m_{\chi}$. Hence the branching ratios can be of the same order if $K_\gamma = \mathcal{O}(1)$, or we can have a neutralino decaying almost exclusively to the pseudo-goldstino if $K_\gamma \gg 1$. For instance we can have $K_\gamma \sim 100$ and then the decay rate of the neutralino is going to be $10^4$ times larger with respect to a single sector scenario.

In order for the neutralino to decay inside the detector, its total width cannot be too small. A rough order of magnitude of the bound is $\Gamma_{\text{tot}} \gtrsim 10^{-16}$ GeV. For a single sector scenario and $m_\chi \sim 200$ GeV, it would translate to $\sqrt{F} \lesssim 10^3$ TeV (see e.g. [32]), but in our case the constraint is more flexible due to the presence of the $K_\gamma$ factor.

We now list the partial widths for the decay of the neutralino into a $Z$ boson and a goldstino or a pseudo-goldstino. For the goldstino, using either (17) or (20), one obtains the classic result [31]

$$\Gamma(\chi \to ZG) = \frac{(2a_{Z_T}^2 + a_{Z_L}^2)m_{\chi}^5}{32\pi F^2} \left(1 - \frac{m_Z^2}{m_{\chi}^2}\right)^4.$$  \hspace{1cm} (25)

For the pseudo-goldstino, the decay rate is given by

$$\Gamma(\chi \to ZG') = \frac{\beta}{16\pi m_{\chi}} |\mathcal{M}|^2,$$  \hspace{1cm} (26)

where $\beta \equiv \beta \left(\frac{m_{G'}^2}{m_{\chi}^2}, \frac{m_{G'}^2}{m_{\chi}^2}\right)$ with

$$\beta(a, b) = (1 + a^2 + b^2 - 2a - 2b - 2ab)^{1/2}$$  \hspace{1cm} (27)

is the usual phase space factor and the spin summed and averaged amplitude squared is

$$|\mathcal{M}|^2 = \frac{1}{2F^2} \left\{ (m_{\chi}^2 - m_Z^2)^3(2K_T^2 + K_L^2) + 6m_{G'}m_Z(m_{\chi}^2 - m_Z^2)^2K_TK_L \\
+ m_{G'}^2(m_{\chi}^2 - m_Z^2) \left[(-4m_{\chi}^2 - m_Z^2)K_T^2 + (-2m_{\chi}^2 + m_Z^2)K_L^2 - 6m_{\chi}m_ZK_TK_L\right] \\
- 6m_{G'}^4m_Z \left[m_{\chi}m_Z(K_T^2 + K_L^2) + (m_{\chi}^2 + m_Z^2)K_TK_L\right] \\
+ m_{G'}^4 \left[(2m_{\chi}^2 + m_Z^2)K_T^2 + (m_{\chi}^2 + 2m_Z^2)K_L^2 + 6m_{\chi}m_ZK_TK_L\right] \right\},$$  \hspace{1cm} (28)

where $K_T \equiv K_{Z_T}a_{Z_T}$ and $K_L \equiv K_{Z_L}a_{Z_L}$. The decay channel is open only when $m_{G'} < m_{\chi} - m_Z$.

We note that, upon setting $K_\gamma = K_{Z_T} = K_{Z_L} = 1$, the decay rates to a pseudo-goldstino slightly differ from those to a massive spin-3/2 gravitino, as detailed for instance in [33].
Figure 1: Branching ratios for the lightest neutralino decay into a (pseudo)-goldstino and a photon or $Z$ at the SPS8 benchmark point. On the left the coupling of the pseudo-goldstino to the photon is gradually enhanced, while on the right the case of enhanced coupling of the pseudo-goldstino to the $Z$ boson is shown.

In Fig. 1 we plot the branching ratios for the lightest neutralino decay for varying pseudo-goldstino mass and for various values of $K_\gamma$, $K_{Z_1}$ and $K_{Z_L}$. The remaining relevant SUSY parameters are taken at the SPS8 benchmark point as calculated by SOFTSUSY \cite{34}. Namely, we have $m_G (= m_{3/2}) = 4.74$ eV, $m_\chi = 139.2$ GeV, $N_{11} = 0.99$, $N_{12} = -0.031$, $N_{13} = 0.124$, $N_{14} = -0.048$ and $\tan \beta = 14.5$. In general, the partial widths for decay into $Z$ bosons are very much suppressed with respect to the ones for decay into photons, except when $K_{Z_T}$ and/or $K_{Z_L}$ are the only large factors. In the following we will not assume this. Also, the partial width for decay into higgses is negligible at the SPS8 point. See \cite{16} for a different set up where this is not the case.

It is obvious that the neutralino total width will always be exceedingly small, e.g. $\Gamma_{\text{tot}} \sim 10^{-12}$ GeV for $K_\gamma = K_{Z_T} = K_{Z_L} = 1$, compared to $m_\chi$, so that we can safely place ourselves in the narrow width approximation (NWA) in all processes of interest with an intermediate neutralino. In the next sub-sections we will discuss observable signatures involving the production and decay of neutralinos. Thus, the (differential) cross sections will be proportional to the square of the amplitudes for production of neutralinos, and to the branching ratios for their decay.
3.2 Goldstini and single photon production in $e^+e^-$ collisions

We now perform an analytic computation with the purpose of highlighting the differences with respect to the single sector case and the role played by the extra parameters $K_\lambda$ and $K_\phi$, characterizing the pseudo-goldstino couplings. For simplicity, in this subsection only, we stick to the case where the neutralino is a pure photino, i.e. $a_\gamma = 1$ and $a_{Z_T} = a_{Z_L} = 0$.

There are three kinds of diagrams contributing to this process, as in Fig. 2. In the $s$-channel, the intermediate particle is a photon, since the neutralino is pure photino. Note also that there is another $s$-channel diagram with the outgoing arrows reversed. (We are using the two-component notation of [28].) In the $t$- and $u$-channels, the intermediate particle is either of the right- and left-handed selectrons. We assume here that the factor $K_\phi$ is the same for both selectrons.

The couplings of the (pseudo)-goldstino have been reviewed in section 2 and for a pure photino neutralino they are (see (11) and (12))

$$
\mathcal{L}_{G'} \supset K_\lambda \frac{m_\chi}{2\sqrt{6}M_p m_{3/2}} \lambda \sigma^\mu \bar{\sigma}^\nu G' F_{\mu\nu} + K_\phi \frac{m_{\tilde{e}}^2}{\sqrt{3}M_p m_{3/2}} G' \psi \phi^*,
$$

where $m_{3/2} = F/\sqrt{3}M_p$ is the gravitino mass, $m_{\tilde{e}}$ is the right and left selectron mass (we have neglected the mass of the electron with respect to the mass of the selectrons) and finally $m_\chi \equiv m_\lambda$. The other couplings needed for the computation can be gathered from e.g. [28].

Note that in the amplitude squared all diagrams actually interfere due to the mass of the pseudo-goldstino. The computation is thus more involved than the one for a massless goldstino [35]. The differential cross section for production of a photino and a pseudo-goldstino reads

$$
d\sigma_{e^+e^- \to \chi G'} = \frac{1}{2s} |\mathcal{M}|^2 d\Phi_2.
$$

![Figure 2: All diagrams contributing to $e^+e^- \to \chi G/G'$: a) $s$-channel, b) $t$-channel and c) $u$-channel.](image-url)
with the spin summed and averaged amplitude squared

\[ |\mathcal{M}|^2 = \frac{e^2}{3M_p^2m_{3/2}^2} \left\{ \frac{K_\lambda^2m_\chi^2}{s} \left( 2tu - m_\chi^2(t + u) + 2m_Gm_\chi s + m_{G'}^2(2m_\chi^2 - t - u) \right) \right. \\
+ K_{\phi}^2m_\tilde{e}^4 \left( \frac{(t - m_{G'}^2)(t - m_\chi^2)}{(t - m_\chi^2)^2} + \frac{(u - m_{G'}^2)(u - m_\chi^2)}{(u - m_\chi^2)^2} + \frac{2m_Gm_\chi s}{(t - m_\chi^2)(u - m_\chi^2)} \right) \right. \\
- 2K_\lambda K_{\phi}m_\chi m_\tilde{e}^2 \left( \frac{m_\chi(t - m_{G'}^2)}{t - m_\tilde{e}^2} + \frac{m_{G'}(t - m_\chi^2)}{u - m_\tilde{e}^2} + \frac{m_\chi(u - m_{G'}^2) + m_{G'}(u - m_\chi^2)}{u - m_\tilde{e}^2} \right) \right\},
\]

(31)

where \( e \) is the electromagnetic coupling constant. We refer to e.g. [37] concerning kinematics. One can check that in the limit \( m_{G'} \to 0 \) and \( K_\lambda = K_{\phi} = 1 \) this reproduces the result reported in [36]. Plugging \( |\mathcal{M}|^2 \) in (30) and integrating over \( \cos \theta \) we get the total cross section.

It is interesting to note that the above amplitude is slightly different depending on the relative sign of the respective (real) Majorana masses of the neutralino LOSP and the pseudo-goldstino. This relative sign is model dependent.

It should be stressed that the cross section scales with \( K_\lambda^2/\lambda/m_{3/2}^2 \). In the spirit of [36, 38, 39, 40, 41], LEP bounds on such cross sections can be translated into upper bounds on \( K/m_{3/2} \), or alternatively on \( K \) at a given value of \( m_{3/2} \). (Here \( K \) is for simplicity a common value for \( K_\lambda \) and \( K_{\phi} \).) Roughly, we get \( K < 10^{4-5}(m_{3/2}/eV) \), which allows us some elbow room. Note that in the case of the single true goldstino production, i.e. with \( K_\lambda = K_{\phi} = 1 \), the cross section is very small, unless the gravitino mass is of order \( 10^{-5} - 10^{-4} \) eV [36]. In the case of the pseudo-goldstino, instead, the cross section can be enhanced by the couplings \( K_\lambda \) and \( K_{\phi} \) while keeping the gravitino mass to standard values for gauge mediation scenarios, i.e. \( m_{3/2} \sim eV \).

To exemplify the physics of this process, and in particular the dependence on the pseudo-goldstino parameters, in Fig. 3 we plot the total cross section as a function of the pseudo-goldstino mass for some values of the parameters \( K_\lambda \) and \( K_{\phi} \). Here we consider a photino LOSP and take the masses as \( m_{3/2} = 10^{-9} \) GeV, \( m_\chi = 140 \) GeV and \( m_\tilde{e}_R = m_\tilde{e}_L = 400 \) GeV.

There is a destructive interference between the diagrams and thus the cross section for large \( K_{\phi} \) turns out to be greater than the cross-section when both \( K_\lambda \) and \( K_{\phi} \) are large. We notice that rather large values of \( K_\lambda \) and \( K_{\phi} \) are required to obtain the cross section around \( \mathcal{O}(10^{2-3}) \) fb with the eV order gravitino mass, while such large values are not favored by the stability of the SUSY breaking vacuum as mentioned before.

One can also easily see that in these cases the emitted photons can be significantly softer than in usual gauge mediation scenario, since the pseudo-goldstino has a non negligible mass.
Moreover, similar to the discussions in [42], the photon energy distribution can tell us about the masses of the neutralino and pseudo-goldstino as we will explicitly see in the next section. On the other hand, different $K$ factors would give different photon angular distributions.

All the results presented here can be obtained numerically running MadGraph 5 [43] simulations adapted to the (pseudo)-goldstino scenario (building on [44]), having implemented the model using FeynRules [45, 46, 47]. This provides also a non trivial test of our software package, which we will use afterwards to simulate $pp$ collisions.

3.3 Goldstini and di-photon production in $e^+e^-$ collisions

The production of two neutralinos will lead to a di-photon plus missing energy signature, which is evidence for the processes

$$e^+e^- \rightarrow \gamma\gamma GG, \quad e^+e^- \rightarrow \gamma\gamma GG', \quad e^+e^- \rightarrow \gamma\gamma G'G'. \quad (32)$$

The total cross section ($\sigma_{e^+e^- \rightarrow \chi\chi} \sim 177$ fb at $\sqrt{s} = 500$ GeV at SPS8) is similar to the single sector case, since the couplings that can be enhanced in the pseudo-goldstino scenario only appear in the decay of the neutralinos. However the photon spectrum, and in particular the edges of the energy distribution, is sensitive to the mass of $G'$, both if the branching ratios are comparable or if the decay to $G'$ is favoured.
In Fig. 4, the distributions of the leading photon energy (left) and of the missing invariant mass (right) for $e^+e^- \to \chi\chi \to \gamma\gamma$ at $\sqrt{s} = 500$ GeV are shown. To obtain both plots, we applied a cut on the energy and the rapidity of the photons, $E_\gamma > 15$ GeV and $|\eta_\gamma| < 2$, as the minimal cuts for the detection of photons. In addition, we imposed the invisible invariant mass cut $M_{\text{inv}} > 100$ GeV to remove the SM ($Z \to \nu\bar{\nu})\gamma\gamma$ background. The remaining background comes from the $t$-channel $W$-exchange process, and this can be reduced by using the polarized $e^\pm$ beams.

Besides the reference point $m_{G'} = 0$ with $K_\gamma = 1$ (for which we have essentially two indistinguishable copies of a light goldstino), we take two different pseudo-goldstino masses, 85 GeV and 125 GeV, with different couplings as in the following table:

1a. $m_{G'} = 85$ GeV with $K_\gamma = 1$ $[B(\chi \to \gamma G') \sim 0.2]$
1b. $m_{G'} = 85$ GeV with $K_\gamma = 2$ $[B(\chi \to \gamma G') \sim 0.5]$
1c. $m_{G'} = 85$ GeV with $K_\gamma = 10$ $[B(\chi \to \gamma G') \sim 1]$
2a. $m_{G'} = 125$ GeV with $K_\gamma = 10$ $[B(\chi \to \gamma G') \sim 0.5]$
2b. $m_{G'} = 125$ GeV with $K_\gamma = 100$ $[B(\chi \to \gamma G') \sim 1]$

Here, we keep $K_{Z_L} = K_{Z_T} = 1$, and hence the decay modes into $Z$ are negligible; see also Fig. 1 for the branching ratios. We have also run the simulations for $m_{G'} = 10$ GeV with $K_\gamma = 1, 2$ and 10, for which the branching ratio is respectively 0.5, 0.8 and 1, but we found distributions essentially overlapping with the massless one.

The edges of the energy distributions allow to determine both the mass of the neutralino LOSP and of the pseudo-goldstino. A simple generalization of the massless goldstino case discussed in [31] gives the following expression for the minimal and maximal energy of each emitted photon:

$$E_{\gamma}^{\text{max, min}} = \frac{\sqrt{s}}{4} \left( 1 - \frac{m_{G'}^2}{m_\chi^2} \right) \left( 1 \pm \sqrt{1 - \frac{4m_\chi^2}{s}} \right). \quad (33)$$

In this case, it is difficult to determine the minimal edges due to the detector cut. On the other hand, the $E_\gamma^{\text{max}}$ is rather clear although the edge of the high energy region is smeared by the missing invariant mass cut. It is interesting to note that, unless the branching ratio is not close to unity, we can find the two $E_\gamma^{\text{max}}$ edges with $m_{G'} \neq 0$ and $m_{G'} = 0$, which can determine both $m_\chi$ and $m_{G'}$. Moreover, we can also determine the branching ratio from the shape of the distributions, i.e. the information on the coupling.
Figure 4: The distributions of the leading photon energy (left) and of the missing invariant mass (right) for $e^+e^- \rightarrow \chi \chi \rightarrow \gamma \gamma + E_T$ at $\sqrt{s} = 500$ GeV, where the pseudo-goldstino mass is fixed at 85 GeV (red) and 125 GeV (blue). The $m_{G'} = 0$ case (black) is also shown as the reference point as well as the SM background.

3.4 Goldstini production in pp collisions

We now turn to consider the processes which are relevant to the LHC.

Similar to the process $e^+e^- \rightarrow \chi G'$ in Sec. 3.2, the cross section of $pp \rightarrow \chi G'$ is proportional to $K^2/m_{3/2}^2$ and could be enhanced by the factor $K$. However, rather large $K$ values of $O(10^4-5)$ are needed to obtain a visible cross section for an eV-order gravitino, leading to a bound for the $K$ values by the $\gamma + E_T$ events at the Tevatron [48] similar to the LEP bound discussed above. We note that at the parton level the amplitudes are the same as the ones studied in the previous section after replacing the incoming electrons with the quarks.

The clean $\gamma \gamma + E_T$ signal is given by the neutralino LOSP pair production. However, the cross section is too small ($\sigma_{LO pp \rightarrow \chi \chi} \sim 0.3 (1.2)$ fb at $\sqrt{s} = 7 (14)$ TeV at SPS8) to be significant over the SM background. It is worth to emphasize again that the emitted photons associated with a pseudo-goldstino are softer than those with a true goldstino, which makes it difficult to

---

4Note that only in this process, and the following one, we would need to specify some squark masses. These can also be easily extracted from SPS8, however as we will argue the most interesting process that we study in more details does not involve intermediate coloured superpartners.

5It is well known that the NLO QCD corrections enhance the LO cross section by a factor of 1.3-1.4 for $\sqrt{s} = 14$ TeV [49]. It is also interesting to note that $gg$ collisions can give a certain contribution to the neutralino pair production through one loop [50]. The corresponding amplitudes are suppressed by the loop factor, while they are enhanced because of the larger gluon PDF, and also because all (s)quarks can run in the loop.
apply some cuts to enhance the signal over the background. In other words, the experimental constraints for the SPS8 point in the standard minimal GMSB model as well as for general gauge mediation [23] (e.g. [51, 52, 20, 53, 54]) could be eased in the multiple goldstini scenario.

Among the exclusive processes with at most two extra particles in the final state, the cleanest one is the one where the two photons and missing energy are accompanied by two leptons. By far the main contribution to the signal comes from the pair production of sleptons, which subsequently decay into a lepton and the neutralino LOSP,

$$pp \rightarrow \tilde{l}_R^- \tilde{l}_L^+ \rightarrow l^+ l^- + \gamma\gamma + \not{E}_T$$

($l = e, \mu$). The electron and muon pairs give the same contributions due to the degeneracies between the first two slepton families. The Standard Model background is completely negligible compared to the signal of new physics.

The signal cross section is 1.1 (3.3) fb at $\sqrt{s} = 7 (14)$ TeV at SPS8, where the slepton masses are $m_{\tilde{l}_R/L} = 180.2/358.2$ GeV and we employ the CTEQ6L1 PDFs [55] with the factorization scale chosen as $\mu = (m_{\tilde{l}_R} + m_{\tilde{l}_L})/2$. Here, the leptons and photons are required to have $p_T > 20$ GeV, $|\eta| < 2.5$, and $R_{l\ell,\gamma\gamma} > 0.4$, where $p_T$ and $\eta$ are the transverse momentum and the pseudorapidity of a final-state particle, respectively, and $R_{ij}$ describes the separation of the two particles in the plane of the pseudorapidity and the azimuthal angle.

Because of the peculiarities of hadronic collisions, raising the center-of-mass energy from

---

Figure 5: The $p_T$ distributions of the leading photon for $pp \rightarrow \tilde{l}_R^- \tilde{l}_L^+ \rightarrow l^+ l^- + \gamma\gamma + \not{E}_T$ at $\sqrt{s} = 14$ TeV for $m_{G'} = 85$ GeV (left) and 125 GeV (right). The $m_{G'} = 0$ case is also shown as a reference with black lines.
7 TeV to 14 TeV increases the total cross section but does not alter significantly the shape of the distributions. Therefore, we present the results only for the 14 TeV LHC here. In Figs. 5 and 6, the distributions of the $p_T$ of the leading photon and of the transverse missing energy are shown, respectively, where the same benchmark points are taken as in Sec. 3.3. The SM background is invisibly small. The two plotted variables show different shapes with respect to the standard goldstino scenario ($m_{G'} = 0$) depending on the mass and the coupling of the pseudo-goldstino. This fact could in principle be used to extract the masses and the couplings by using techniques explained in [59, 60, 61, 62]. We note that in the case of $m_{G'} = 125$ GeV the signal cross section is largely reduced by the experimental cuts, especially for large $K_{\gamma}$. This is due to the fact that, for more massive pseudo-goldstino, the emitted photons will be softer, and hence more excluded by the kinematical cuts.

Before closing the section, we note that the production cross sections of the colored SUSY particles at SPS8 are small due to their large masses in the TeV range. In general, although we have presented the exclusive signals without jets here, the inclusive search is also interesting and will be reported elsewhere.

4 The case of the stau LOSP

We now move on to the case where the $\tilde{\tau}$ is the LOSP, and use the Lagrangian (22) to study it. The effect of the coefficients $K_{\tau_L}$ and $K_{\tau_R}$ is that of enhancing the $G'$ production.
4.1 Decays of the stau

The decay amplitude squared for the process $\tilde{\tau} \to \tau G'$ can be easily computed in terms of the coefficients in the Lagrangian yielding

$$|M|^2 = \left(\frac{m^2_{\tilde{\tau}} - m^2_\tau}{F}\right)^2 \left((K_{\tau L}^2 \cos^2 \theta_{\tilde{\tau}} + K_{\tau R}^2 \sin^2 \theta_{\tilde{\tau}})(m^2_{\tilde{\tau}} - m^2_{G'} - m^2_\tau)ight) + 4K_{\tau L} K_{\tau R} \sin \theta_{\tilde{\tau}} \cos \theta_{\tilde{\tau}} m_{G'} m_{\tau}). \quad (34)$$

The width can be written as

$$\Gamma(\tilde{\tau} \to \tau G') = \frac{\beta}{16\pi m_{\tilde{\tau}}} |M|^2 \quad (35)$$

with $\beta \equiv \beta(m^2_{\tilde{\tau}}/m^2_\tau, m^2_{G'}/m^2_\tau)$ as in (27). Notice that the width depends not only on the magnitude but also on the ratio of the coefficients $K_{\tau L}$ and $K_{\tau R}$. The well known expression for the true goldstino case is obtained from the above by simply setting $K_{\tau L} = K_{\tau R} = 1$ and $m_{G'} = 0$.

For illustration we plot the branching ratios of the decay $\tilde{\tau} \to \tau G'$, choosing the stau mass and mixing angle given by the SPS7 benchmark point, namely $m_{\tilde{\tau}} = 124.0$ GeV and $\cos \theta_{\tilde{\tau}} = 0.154$. The smallness of $\cos \theta_{\tilde{\tau}}$ at the SPS7 point makes the branching ratio largely independent from $K_{\tau L}$ but this would of course change for a different mixing angle.
Figure 8: The distributions of $p_T$ of the leading tau (left) and of the missing transverse energy (right) for $pp \to \tilde{\tau}^+\tilde{\tau}^- \to \tau^+\tau^- + E_T$ at $\sqrt{s} = 14$ TeV for $m_{G'} = 85$ GeV. The $m_G = 0$ case (black) is also shown as the reference point as well as the SM background.

The total width of the stau LOSP at SPS7, where $m_G (= m_{3/2}) = 0.76$ eV, is of the order of $10^{-10}$ GeV for $K_{\tau L} = K_{\tau R} = 1$, and hence the stau will decay promptly into the detector. Scenarios with long lived staus could also be envisioned, with even the possibility of stopping them and then measuring their decays. In that case the branching ratio and the mass of the invisible particle(s) should be more directly accessible. We will not delve further on this scenario.

4.2 Goldstini and di-tau production

We now turn to stau production at colliders and subsequent decay into taus and (pseudo)-goldstini. Though we could first consider stau pair production at $e^+e^-$ colliders, we will omit this rather straightforward exercise. In the neutralino LOSP scenario, the benefit of this set up was the ability to infer the neutralino and pseudo-goldstino masses from the energy distribution of the emitted photons. In the present case the same considerations are practically harder to achieve because of the difficulties inherent in tau reconstruction. We thus proceed to consider directly the case of hadron colliders.

The process we are interested in is $pp \to \tilde{\tau}^+\tilde{\tau}^- \to \tau^+\tau^- + E_T$. The lighter stau-pair production cross section at SPS7 is 41 fb at $\sqrt{s} = 14$ TeV\footnote{See footnote 6 and also \cite{B3} for more details on the stau-pair production.} while the irreducible SM background $\tau^+\tau^-\nu\bar{\nu}$, mainly coming from $Z$ and $W$ pair productions, is ten times larger with the minimal
Table 1: Cross sections for the signals and the background. The significance $S$ in (36) is calculated with an integrated luminosity of 100 (30) fb$^{-1}$ and a di-tau detection efficiency $A = 0.1$.

cuts $p_T > 20$ GeV, $|\eta| < 2.5$, and $R_{\tau\tau} > 0.4$. Since the background is located in the low tau-tau invariant mass region, we impose the additional cut $M_{\tau\tau} > 150$ GeV in the analyses below.

Figure 8 shows the distributions of the $p_T$ of the leading tau and of the missing transverse energy for the following benchmark points covering different branching ratios for stau decays into $G$ or $G'$:

1a. $m_{G'} = 85$ GeV with $K_{\tau_L} = K_{\tau_R} = 1$  
    $[B(\tilde{\tau} \to \tau G') \sim 0.2]$

1b. $m_{G'} = 85$ GeV with $K_{\tau_L} = K_{\tau_R} = 2$  
    $[B(\tilde{\tau} \to \tau G') \sim 0.5]$

1c. $m_{G'} = 85$ GeV with $K_{\tau_L} = K_{\tau_R} = 10$  
    $[B(\tilde{\tau} \to \tau G') \sim 1]$

The reference point $m_{G'} = 0$, i.e. the standard goldstino scenario, is also shown by a black solid line. As in the neutralino LOSP scenario, a sizable branching ratio of stau decays to pseudo-goldstini has an impact on the shape of the distribution, once again making the spectrum softer. Another noticeable fact is that the new physics signal becomes dominant especially for high missing transverse energy only when the stau decays to true goldstinos are significant. Therefore, the pseudo-goldstini scenario makes it harder to achieve enough significance for its observation.

In order to quantify the sensitivity of the missing transverse energy cut, in Tables 1 and 2 we list the cross sections, signal ($s$) over background ($b$) and significances ($S$) for our benchmarks, without and with a cut on $E_T$ at 100 GeV respectively. Taking into account the branching ratio of the hadronic tau decays, $B(\tau_{had}) = 0.648$ [37], and the efficiency of the hadronic tau identification, $\epsilon = 0.5$ [64, 65], we assume the di-tau detection efficiency $A = (B(\tau_{had}) \times \epsilon)^2 \sim 0.1$. We use the signal significance defined as [66]

$$S = \sqrt{2((s + b) \ln(1 + s/b) - s)}.$$  (36)
We observe that for 100 fb$^{-1}$ of integrated luminosity, a satisfactory significance can be achieved for most of our benchmarks, especially for $E_T > 100$ GeV. However, in the $K_\tau = 10$ case, i.e. in the case of the heavy pseudo-goldstino with the enhanced coupling, the cut on $E_T$ does not improve the significance of the signal.

Finally we note that, although we took $K_{\tau L} = K_{\tau R}$ for simplicity, tau polarization may be exploited to determine the case that the two coefficients are different, $K_{\tau L} \neq K_{\tau R}$ [67].

5 Conclusions

In this paper we have analyzed how the traditional expectations from a low scale gauge mediated model can be modified by the presence of a massive pseudo-goldstino NLSP in a scenario with multiple-sector SUSY breaking.

We first considered the case of a gaugino-like neutralino LOSP. We showed that the decay modes of the LOSP into a photon or $Z$-boson and a pseudo-goldstino can be significant. We studied in details the goldstini phenomenology in the photon(s) plus missing energy signals in $e^+e^-$ and $pp$ collisions. Our aim was to provide clues to interpret prompt photon plus missing energy signals at the LHC. We found that the resulting photon spectrum is typically softer and with different shapes, compared to the standard gauge mediation scenario with only one hidden sector.

We then proceeded to consider the case of a stau LOSP. Similarly to the previous case, the stau can significantly decay into a tau and a pseudo-goldstino. We studied a possible tau pair plus missing energy signal at the LHC, again finding that the pseudo-goldstino scenario leads to an altered shape in the tau energy distributions. The signature however seems more promising in the neutralino LOSP scenario, not only because photons have cleaner experimental features than taus, but also because the SM background is virtually absent in the process that we studied.
Although we performed our analyses at the particular benchmark points (SPS8 for $\chi$ LOSP and SPS7 for $\tilde{\tau}$ LOSP) to make a comparison with the standard gauge mediation model, our goldstini model can be easily extended to other benchmark points and LOSP scenarios due to the implementation into a event generator, MadGraph 5. We emphasized the dependence of the experimental signatures on the new parameters, namely the pseudo-goldstino mass and its couplings. A rather model independent feature of the pseudo-goldstini scenario is that it provides a scenario which is fully consistent with gauge mediation of supersymmetry breaking, while it softens significantly the energy of the SM products of the LOSP decays, due to the conspicuous mass of the pseudo-goldstino. In this way such a scenario evades most experimental bounds that tend to exclude gauge mediated scenarios.

We would like to suggest that models like the one we have presented here, where the missing energy is carried away by two different particles, one rather massive and the other almost massless, and with similar couplings but with different strength, deserve to be considered in LHC data analysis.

Acknowledgments

We would like to thank H. Haber, Z. Komargodski, F. Maltoni, N. Seiberg and J. Thaler for stimulating discussions. We are also grateful to J. Alwall, R. Frederix and O. Mattelaer for help with MadGraph, to C. Duhr and B. Fuks for help with FeynRules, and to F. Blekman and H. Yokoya for suggestions on the tau detection. Y.T would like to thank Fabio Maltoni and the members of the CP3, Universite Catholique de Louvain for their warm hospitality, where a part of this work was done.

The research of R.A. is supported in part by IISN-Belgium (conventions 4.4511.06, 4.4505.86 and 4.4514.08). R.A. is a Research Associate of the Fonds de la Recherche Scientifique-F.N.R.S. (Belgium). The research of G.F. is supported in part by the Swedish Research Council (Vetenskapsrådet) contract 80409701. A.M. is a Postdoctoral Researcher of FWO-Vlaanderen. A.M. is also supported in part by FWO-Vlaanderen through project G.0428.06. K.D.C. and K.M. are supported by the Concerted Research action “Supersymmetric Models and their Signatures at the LHC” of the Vrije Universiteit Brussel. R.A., K.D.C, A.M. and K.M. are supported in part by the Belgian Federal Science Policy Office through the Interuniversity Attraction Pole IAP VI/11. Y.T. was also supported in part by Sokendai short-stay study abroad program.
References

[1] S. Chatrchyan et al. [ CMS Collaboration ], arXiv:1109.2352 [hep-ex].

[2] G. Aad et al. [ ATLAS Collaboration ], arXiv:1109.6572 [hep-ex].

[3] G. Aad et al. [ ATLAS Collaboration ], arXiv:1109.6606 [hep-ex].

[4] T. Aaltonen et al. [CDF Collaboration], Phys. Rev. Lett. 104 (2010) 011801 arXiv:0910.3606 [hep-ex].

[5] S. Chatrchyan et al. [ CMS Collaboration ], Phys. Rev. Lett. 106 (2011) 211802. arXiv:1103.0953 [hep-ex].

[6] S. Chatrchyan et al. [ CMS Collaboration ], JHEP 1106 (2011) 093. arXiv:1105.3152 [hep-ex].

[7] G. Aad et al. [ ATLAS Collaboration ], arXiv:1107.0561 [hep-ex].

[8] G. Aad et al. [ATLAS Collaboration], arXiv:1111.4116 [hep-ex].

[9] C. Cheung, Y. Nomura and J. Thaler, JHEP 1003 (2010) 073 arXiv:1002.1967 [hep-ph].

[10] C. Cheung, J. Mardon, Y. Nomura and J. Thaler, JHEP 1007 (2010) 035 arXiv:1004.4637 [hep-ph].

[11] K. Benakli and C. Moura, Nucl. Phys. B 791 (2008) 125 arXiv:0706.3127 [hep-th].

[12] N. Craig, J. March-Russell and M. McCullough, JHEP 1010 (2010) 095 arXiv:1007.1239 [hep-ph].

[13] M. McCullough, Phys. Rev. D 82 (2010) 115016 arXiv:1010.3203 [hep-ph].

[14] H. -C. Cheng, W. -C. Huang, I. Low and A. Menon, JHEP 1103 (2011) 019 arXiv:1012.5300 [hep-ph].

[15] K. I. Izawa, Y. Nakai and T. Shimomura, JHEP 1103 (2011) 007 arXiv:1101.4633 [hep-ph].

[16] J. Thaler, Z. Thomas, JHEP 1107 (2011) 060. arXiv:1103.1631 [hep-ph].
[17] C. Cheung, F. D’Eramo and J. Thaler, JHEP 1108 (2011) 115 [arXiv:1104.2600 [hep-ph]].
[18] D. Bertolini, K. Rehermann, J. Thaler, [arXiv:1111.0628 [hep-ph]].
[19] R. Argurio, Z. Komargodski and A. Mariotti, Phys. Rev. Lett. 107 (2011) 061601 [arXiv:1102.2380 [hep-th]].
[20] P. Meade, M. Reece and D. Shih, JHEP 1005 (2010) 105 [arXiv:0911.4130 [hep-ph]].
[21] C. Petersson, A. Romagnoni and R. Torre, arXiv:1203.4563 [hep-ph].
[22] B. C. Allanach, M. Battaglia, G. A. Blair, M. S. Carena, A. De Roeck, A. Dedes, A. Djouadi and D. Gerdes et al., Eur. Phys. J. C 25 (2002) 113 [hep-ph/0202233].
[23] P. Meade, N. Seiberg and D. Shih, Prog. Theor. Phys. Suppl. 177 (2009) 143 [arXiv:0801.3278 [hep-ph]].
[24] T. Aaltonen et al. [CDF Collaboration], Phys. Rev. Lett. 104 (2010) 011801 [arXiv:0910.3606 [hep-ex]].
[25] V. M. Abazov et al. [D0 Collaboration], Phys. Rev. Lett. 105 (2010) 221802 [arXiv:1008.2133 [hep-ex]].
[26] G. F. Giudice and R. Rattazzi, Phys. Rept. 322 (1999) 419 [arXiv:hep-ph/9801271].
[27] P. Fayet, Phys. Lett. B70 (1977) 461.
[28] H. K. Dreiner, H. E. Haber and S. P. Martin, Phys. Rept. 494 (2010) 1 [arXiv:0812.1594 [hep-ph]].
[29] F. Luo, K. A. Olive, M. Peloso, JHEP 1010 (2010) 024. [arXiv:1006.5570 [hep-ph]].
[30] Z. Komargodski and N. Seiberg, JHEP 0909 (2009) 066 [arXiv:0907.2441 [hep-th]].
[31] S. Ambrosanio, G. L. Kane, G. D. Kribs, S. P. Martin and S. Mrenna, Phys. Rev. D 54, 5395 (1996) [arXiv:hep-ph/9605398].
[32] S. P. Martin, arXiv:hep-ph/9709356
[33] J. L. Feng, S. Su and F. Takayama, Phys. Rev. D 70 (2004) 075019 [hep-ph/0404231].
[34] B. C. Allanach, Comput. Phys. Commun. 143 (2002) 305 [hep-ph/0104145].
[35] P. Fayet, Phys. Lett. B 175 (1986) 471.

[36] J. L. Lopez, D. V. Nanopoulos and A. Zichichi, Phys. Rev. D 55, 5813 (1997) [arXiv:hep-ph/9611437].

[37] K. Nakamura et al. [Particle Data Group Collaboration], J. Phys. G G 37 (2010) 075021.

[38] D. A. Dicus and S. Nandi, Phys. Rev. D 56, 4166 (1997) [arXiv:hep-ph/9611312].

[39] A. Brignole, F. Feruglio and F. Zwirner, Nucl. Phys. B 516, 13 (1998) [Erratum-ibid. B 555, 653 (1999)] [arXiv:hep-ph/9711516].

[40] P. Achard et al. [L3 Collaboration], Phys. Lett. B587, 16-32 (2004). hep-ex/0402002.

[41] J. Abdallah et al. [DELPHI Collaboration], Eur. Phys. J. C 38 (2005) 395 [hep-ex/0406019].

[42] K. Mawatari, B. Oexl, Y. Takaesu, Eur. Phys. J. C71 (2011) 1783. arXiv:1106.5592 [hep-ph].

[43] J. Alwall, M. Herquet, F. Maltoni, O. Mattelaer, T. Stelzer, JHEP 1106 (2011) 128. arXiv:1106.0522 [hep-ph].

[44] K. Mawatari, Y. Takaesu, Eur. Phys. J. C71 (2011) 1640. arXiv:1101.1289 [hep-ph].

[45] N. D. Christensen, C. Duhr, Comput. Phys. Commun. 180 (2009) 1614-1641. arXiv:0806.4194 [hep-ph].

[46] C. Duhr, B. Fuks, Comput. Phys. Commun. 182 (2011) 2404-2426. arXiv:1102.4191 [hep-ph].

[47] C. Degrande, C. Duhr, B. Fuks, D. Grellscheid, O. Mattelaer, T. Reiter, arXiv:1108.2040 [hep-ph].

[48] D. Acosta et al. [CDF Collaboration], Phys. Rev. Lett. 89 (2002) 281801 arXiv:hep-ex/0205057.

[49] W. Beenakker, M. Klasen, M. Kramer, T. Plehn, M. Spira and P. M. Zerwas, Phys. Rev. Lett. 83 (1999) 3780 [Erratum-ibid. 100 (2008) 029901] arXiv:hep-ph/9906298.
[50] J. Yi, W. G. Ma, L. Han, Z. H. Yu and H. Pietschmann, Phys. Rev. D 62 (2000) 035006 [arXiv:hep-ph/0003291].

[51] S. Abel, M. J. Dolan, J. Jaeckel and V. V. Khoze, JHEP 0912 (2009) 001 [arXiv:0910.2674 [hep-ph]].

[52] S. Abel, M. J. Dolan, J. Jaeckel and V. V. Khoze, JHEP 1012 (2010) 049 [arXiv:1009.1164 [hep-ph]].

[53] J. T. Ruderman and D. Shih, arXiv:1103.6083 [hep-ph].

[54] Y. Kats, P. Meade, M. Reece, D. Shih, arXiv:1110.6444 [hep-ph].

[55] J. Pumplin, D. R. Stump, J. Huston, H. L. Lai, P. M. Nadolsky and W. K. Tung, JHEP 0207 (2002) 012 [arXiv:hep-ph/0201195].

[56] H. Baer, B. W. Harris and M. H. Reno, Phys. Rev. D 57 (1998) 5871 [hep-ph/9712315].

[57] F. del Aguila and L. Ametller, Phys. Lett. B 261 (1991) 326.

[58] F. Borzumati and K. Hagiwara, JHEP 1103 (2011) 103 [arXiv:0912.0454 [hep-ph]].

[59] C. G. Lester and D. J. Summers, Phys. Lett. B 463 (1999) 99 [hep-ph/9906349].

[60] D. R. Tovey, JHEP 0804 (2008) 034 [arXiv:0802.2879 [hep-ph]].

[61] A. J. Barr and C. G. Lester, J. Phys. GG 37 (2010) 123001 [arXiv:1004.2732 [hep-ph]].

[62] H. -C. Cheng and J. Gu, JHEP 1110 (2011) 094 [arXiv:1109.3471 [hep-ph]].

[63] J. M. Lindert, F. D. Steffen and M. K. Trenkel, JHEP 1108 (2011) 151 [arXiv:1106.4005 [hep-ph]].

[64] [CMS Collaboration], CMS-PAS-TAU-11-001.

[65] [ATLAS Collaboration], ATLAS-CONF-2011-077

[66] G. Cowan, K. Cranmer, E. Gross and O. Vitells, Eur. Phys. J. C 71 (2011) 1554 [arXiv:1007.1727 [physics.data-an]].

[67] S. Y. Choi, K. Hagiwara, Y. G. Kim, K. Mawatari and P. M. Zerwas, Phys. Lett. B 648 (2007) 207 [hep-ph/0612237].

27