The Josephson effect describes the flow of supercurrent in a weak link—such as a tunnel junction, nanowire or molecule—between two superconductors. It is the basis for a variety of circuits and devices, with applications ranging from medicine to quantum information. Experiments using Josephson circuits that behave like artificial atoms are now revolutionizing the way we probe and exploit the laws of quantum physics. Microscopically, the supercurrent is carried by Andreev pair states, which are localized at the weak link. These states come in doublets and have energies inside the superconducting gap. Existing Josephson circuits are based on properties of just the ground state of each doublet, and so far the excited states have not been directly detected. Here we establish their existence through spectroscopic measurements of superconducting atomic contacts. The spectra, which depend on the atomic configuration and on the phase difference between the superconductors, are in complete agreement with theory. Andreev doublets could be exploited to encode information in novel types of superconducting qubits.

A bulk, isolated Bardeen–Cooper–Schrieffer superconductor can be described by a density of states (DOS) having a gap around the Fermi energy of $2A$, which is the minimum energy necessary to excite an electron pair. In the presence of a short weak link, the superconducting phase can be easily twisted, leading to a local modification of the DOS and the creation of new states inside the gap. These Andreev bound states have energies $\pm E_A$, with $E_A$ given by

$$E_A = \Delta \sqrt{1 - \tau \sin^2(\delta/2)}$$

for a weak link which has a phase difference $\delta$ across it and a single conduction channel of transmission probability $\tau$ (Fig. 1a). As long as $E_A < \Delta$, these states cannot propagate into the bulk superconductor and are bound to the weak link, over a distance of order $\xi$, the superconducting coherence length. The ground Andreev pair state $| - \rangle$ has energy $-E_A$, and the lowest possible pair excitation of the system, requiring an energy $2E_A$, is a transition to the excited Andreev pair state $| + \rangle$ at $+E_A$. The phase dependence of $\mp E_A$ gives rise to opposite supercurrents for the two states, $\pm (2\pi/\phi_0)(\partial E_A/\partial \delta)$, with $\phi_0 = h/2e$ the flux quantum ($h$ is Planck’s constant, and $e$ the charge of an electron).

Current Josephson circuits are primarily based on tunnel Josephson junctions, which have many conduction channels with small transmission probabilities ($\tau \ll 1$). In this limit, the ground state energy $-E_A$ in each channel is proportional to $-\cos \delta$. Summing over all channels, one recovers the standard Josephson coupling energy $-E_0 \cos \delta$ and the sinusoidal current–phase relation predicted by Josephson’s formula. For channels of arbitrary transmissions, the ground state $| - \rangle$ has been probed by measurements of the current–phase relation in superconducting atomic contacts. Excitations created by the addition or removal of an electron from the state $| - \rangle$ have been observed in superconducting atomic contacts and quantum dots connected to superconductors. The continuum of Andreev states that form in superconductor–normal–superconductor structures has also been probed. Thermal occupation of the excited states was invoked to explain the temperature dependence of the supercurrent. However, the excited Andreev pair state $| + \rangle$ has not been directly detected. Here we present spectroscopic evidence of excited Andreev pair states in superconducting atomic contacts.
contacts, a simple system that allows direct quantitative comparison with theoretical predictions.

The principle of our experiment is described in Fig. 1b. An atomic contact obtained using a microfabricated, mechanically controllable break junction21 is placed in parallel with a tunnel Josephson junction to form a SQUID (superconducting quantum interference device). A second tunnel junction, the 'spectrometer', is used as an on-chip broadband microwave source and detector22–24. It is coupled to the barrier26,27, as in Fig. 1c. In the current–voltage characteristic of the spectrometer junction, a transition of energy E is revealed as a d.c. current peak at 2eV = E with height I = 2I(E), where I(E) is the photon absorption rate. Classically, this rate is related to the real part of the impedance seen by the spectrometer. The on–chip coupling capacitor and LC filtering are designed to keep the absorption rate due to the external environment low. Transitions such as the Andreev excitation (|−⟩→|+⟩) at the energy 2eV = 2EΔ(δ,τ) can be distinguished by their dependence on both the flux and the contact configuration.

Figure 2 shows the current–voltage characteristic I(VJ) of the spectrometer coupled to the SQUID with atomic contact AC2 (see below) at two values of the reduced flux φ. Several current peaks are visible below the voltage 1/4e ≈ 180 μV, which corresponds to the maximum excitation energy of interest for the Andreev transition, 2eV = 2A. Parts of the spectra change by as much as 200 pA as a function of reduced flux φ. When biased at a voltage VJ, the spectrometer undergoes Josephson oscillations and acts as a microwave current source at frequency νJ = 2eVJ/h. Microwave photons emitted by the spectrometer are absorbed by the environment, which subsequently relaxes. The dissipated power P requires a d.c. current I to be supplied by the biasing circuit to satisfy power conservation, P = IJ. Microscopically, this d.c. current is a result of inelastic Cooper-pair tunnelling: each time a photon is absorbed, a Cooper pair tunnels across the spectrometer insulating barrier26,27, as in Fig. 1c. In the current–voltage IJ(VJ) characteristic of the spectrometer junction, a transition of energy E is revealed as a d.c. current peak at 2eVJ = E with height IJ = 2J(E), where J(E) is the photon absorption rate. Classically, this rate is related to the real part of the impedance seen by the spectrometer. The on–chip coupling capacitor and LC filtering are designed to keep the absorption rate due to the external environment low. Transitions such as the Andreev excitation (|−⟩→|+⟩) at the energy 2eVJ = 2EΔ(δ,τ) can be distinguished by their dependence on both the flux and the contact configuration.

Figure 2 | I(VJ) characteristics of the spectrometer coupled to the SQUID with atomic contact AC2. a. Data taken over a large range of VJ. The boxed region is shown magnified in b. b. The sub-gap current for two values of the reduced flux φ. The grey regions at VJ ≈ 9 μV and on the right-hand side of the peak at VJ ≈ 50 μV are not accessible because the biasing is unstable (see main text). The parts of the spectra that change with φ reveal energy absorption by the SQUID.

Figure 3 | Absorption spectra for three atomic contacts. a, AC1 (with two channels of transmission probability, 0.942 and 0.26); b, AC2 (with two channels of transmission probability, 0.985 and 0.37); c, AC3 (more than 20 channels). The colour encodes the current IJ through the spectrometer (colour scale in c applies to all three panels), as a function of the reduced flux φ and of the bias voltage VJ. The right axis gives the spectrometer frequency νJ associated with VJ.

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background which is subtracted from the current–voltage curves (Supplementary Information section 2.2). In Fig. 2b there are no data in the two grey regions ($V_I \approx 50 \mu V$ and $V_I \approx 9 \mu V$) because the spectrometer voltage biasing is not stable (see Methods). The measured current decreases about an order of magnitude as the bias voltage is increased and passes through the zone of instability at $V_I \approx 50 \mu V$.

Spectra measured for the three different atomic contacts AC1, AC2 and AC3 are shown in Fig. 3a–c. In each spectrum, the current $I_i$ through the spectrometer junction is plotted with the common colour scale of Fig. 3c. The vertical axes give the energy of photons emitted by the spectrometer in units of the bias voltage, $h\nu = 2eV_I$. The corresponding frequencies range from 0 to 85 GHz. The horizontal axes give the applied reduced flux, $\phi = \Phi / \Phi_0$, as well as $\phi$, the Andreev transitions. To confirm this, we plot with red lines in Fig. 4b (AC1) and Fig. 4d (AC2) the expected positions $2E_{A1}$ and $2E_{A2}$ of the Andreev transitions using equation (1) for the two highest transmission channels in each contact: AC1 (transmissions 0.942, 0.26) and AC2 (transmissions 0.985, 0.37) (see Supplementary Fig. 3). The lines match the observed transitions.

In addition to the Andreev transitions, there is in Fig. 3a–c a much brighter spectroscopic line ($I_i > 1 \text{nA}$, colour scale red) common to all contacts which is located at 0.51 $\phi$ and hardly varies with flux for AC1 and AC2 but dips to 0.4 $\phi$ for AC3. It corresponds to the large peak at $V_I = 45 \mu V$ in Fig. 2, whose upper half falls in the region of instability. We identify it as the excitation of the plasma mode of the SQUID. This oscillator mode, formed by the SQUID Josephson inductance $L_S(\phi)$ and its parallel capacitance $C_p$, resonates at frequency $\nu_p = (2\pi/\sqrt{L_SC_p})^{-1} \approx 22 \text{ GHz}$ (0.51 $\phi/\hbar$). The capacitance $C_p \approx 280 \text{ fF}$ is the sum of the SQUID and spectrometer capacitances. $L_S(\phi)$ results from the parallel combination of three inductive elements: the atomic contact, the SQUID Josephson junction, and an on-chip inductor on the biasing line (Supplementary Fig. 1). The flux dependence of $L_S(\phi)$ is negligible for the asymmetric SQUIDs (cases AC1, AC2) but results in a 0.1 $\phi$ amplitude modulation (4 GHz) of the plasma frequency for the large atomic-contact SQUID (case AC3). The energy $h\nu_p$, associated with the plasma frequency $\nu_p$, for AC1 and AC2 is plotted in Fig. 4b and d, respectively, as blue lines, and agrees with the experimental data. The abrupt decrease in spectrometer signal above the plasma frequency (Fig. 2b) is due to the shunting of emitted microwaves by the capacitance $C_p$.

The combination of the Andreev and plasma degrees of freedom leads to a double ladder energy diagram, as shown in Fig. 4a. The states are labelled by $(\sigma, n)$, where $\sigma = \pm$ accounts for the Andreev pair state and $n$ is the plasmon number. The data are well explained by considering transitions only from the initial state $|-, n\rangle$. The Andreev transition $|-, n\rangle \rightarrow |+, n\rangle$ is represented by the red arrow and the plasma transition $|-, n\rangle \rightarrow |+, n\rangle$ at $2eV_I = 2E_{A1}$ is represented by the blue arrow.

In the spectrum of each channel, there is another resonance near 1.02 $\phi$, which is similar in shape to the plasma transition but at twice the energy and of smaller amplitude (~100 pA). This corresponds to the second harmonic of the plasma transition, $2eV_I = 2h\nu_p$ (Figs 4b and d, blue dashed line), in which each Cooper pair tunnelling through the spectrometer emits two photons of energy $h\nu_p$. This two-photon plasma transition $|-, n\rangle \rightarrow |-, n\rangle$ is represented by the blue dashed arrow in the energy ladder, Fig. 4a. It is also possible to simultaneously excite the Andreev transition and the plasma mode (Fig. 4a, purple dashed arrow). This type of transition $|-, n\rangle \rightarrow |+, n\rangle$, at $2eV_I = 2E_{A1} + h\nu_p$, is observed in the spectra, Fig. 4b and d, as a replica of the Andreev transition, shifted up by the plasma energy (purple dashed line). These transitions agree with the data everywhere except where two such two-photon processes coincide, near $\phi = \pi$ and $2eV_I \approx 1.02 \phi$. There one observes a level repulsion (Fig. 3a) or an avoided crossing (Fig. 3b), depending on the relative position of the undressed states. In the spectra the region of instability obscures the hybridization effects at energy $2eV_I = h\nu_p$, but line traces slightly below confirm their existence (see Supplementary Information).

The experimental spectra are well described by a model based on the Andreev Hamiltonian (Supplementary Information section 2.3). The eigenenergies of the SQUID Hamiltonian are determined by perturbation analysis and numerical diagonalization. The resulting transition

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**Figure 4 | Interpretation of the absorption spectra.** a. Energy spectrum diagrams for a single channel: each state is labelled $|-, n\rangle$ or $|+, n\rangle$ for the Andreev pair in the ground $(-)$ or excited $+$ state and $n$ photons in the plasma mode. b–e. Predicted transitions between the states shown in a using the bare Andreev and plasma energies (b, d) or by diagonalization of the full Hamiltonian (c, e), for contacts AC1 (b, c) and AC2 (d, e). b, d. Red lines, transition energies $2E_{A1}$ predicted from the channel transmissions (equation (1): $2E_{A1}$ for first channel and $2E_{A2}$ for second channel). Blue lines, excitation energy for the plasma mode $h\nu_p$. Blue dashed line, two-photon plasma mode process $2h\nu_p$. Purple dashed line, two-photon process $2E_{A1} + h\nu_p$, exciting both the Andreev and plasma transitions. c, e. Black lines, calculated transition lines superimposed on the data.
energies are shown as black lines in Fig. 4c and e. Only crossings of transition lines involving the same number of photons show significant hybridization, in good agreement with the data. The rich structure predicted in the top part of the spectrum is not visible in the experiment because of the shunting by the SQUID capacitor. A quantitative description of the intensity and width of the transitions would require taking into account the coupling to the detector and the sources of dissipation.

Our results show that in addition to the phase difference, each conduction channel of a Josephson weak link possesses an internal degree of freedom similar to a spin-1/2. This Andreev pseudo-spin is unique as a microscopic degree of freedom intrinsically coupled to a superconducting circuit and whose energy is tunable over a wide range. Theoretical proposals for an Andreev qubit are based either directly on this pseudo-spin\textsuperscript{11} or on the actual spin of quasiparticles trapped in the Andreev levels\textsuperscript{12,13,16}. Their implementation requires reducing external sources of decoherence, something that could be achieved, in the circuit quantum electrodynamics approach, by integrating a superconducting atomic contact in a high-quality resonator\textsuperscript{28,29}. Finally, in hybrid systems where spin–orbit and Zeeman interactions are also present, Andreev levels give rise to Majorana states whose detection is currently the subject of intense study\textsuperscript{30}.

**METHODS SUMMARY**

The sample is mounted in a bending mechanism (Supplementary Fig. 2d) anchored to the mixing chamber of a dilution refrigerator at 30 mK and housed inside a superconducting shield to reduce magnetic interference. Two microwave launchers connect it to the biasing and measuring lines which are heavily filtered. An electrically shielded small superconducting coil located directly above the sample is used to apply magnetic flux. A microfabricated atomic-size contact configuration. The atomic contacts, tunnel junctions, and on-chip filters (alumina dielectric) are fabricated by electron-beam lithography and evaporation. Tunnel junctions are formed by double-angle evaporation and oxidation and have a bare plasma frequency of 14 GHz. Measurements of the SQUID and spectrometer current–voltage characteristics are made at low frequency (10–100 Hz) with room-temperature amplification. When the differential conductance of the spectrometer is smaller than $-1/R_\text{b}$, the biasing resistor of the spectrometer (see Fig. 1b), such as on the negative-slope side of the first plasma peak, biasing is unstable. This result is in the absence of data in the grey regions above the plasma transition in Figs 2 and 3. At low voltages, there is another instability due to retrapping to the zero-voltage state. The peaks in the current–voltage curves which do not depend on the flux are subtracted from the measured spectra in the region $V_J > 50 \mu V$ as described in Supplementary Information section 2.2. The theoretical spectra of Figs 4c and e are obtained by numerical diagonalization of the Hamiltonian describing both the Andreev states and the plasma mode, which are coupled because they share the phase across the SQUID Josephson junction (Supplementary Information section 2.3).

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Erratum: Exciting Andreev pairs in a superconducting atomic contact
L. Bretheau, Ç. Ö. Girit, H. Pothier, D. Esteve & C. Urbina

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In the colour scale of Fig. 3 of this Letter, the labels for the current $I_I$ should read 1 nA, 0.1 nA and 0.01 nA from top to bottom. This error has been corrected online in the HTML and PDF versions of the paper.