VELOCITY ANISOTROPY AND SHAPE BIAS IN THE CAUSTIC TECHNIQUE

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Abstract

We use the Millennium Simulation to quantify the statistical accuracy and precision of the escape-velocity technique for measuring cluster-sized halo masses at $z \sim 0.1$. We show that in three dimensions one can measure nearly unbiased ($\lesssim 4\%$) halo masses ($\gtrsim 1.5 \times 10^{14} M_{\odot} h^{-1}$) with $10\%$--$15\%$ scatter. Line-of-sight projection effects increase the scatter to $\sim 25\%$, where we include the known velocity anisotropies. The classical “caustic” technique incorporates a calibration factor that is determined from $N$-body simulations. We derive and test a new implementation that eliminates the need for calibration and utilizes only the observables: the galaxy velocities with respect to the cluster mean $v$, the projected positions $r_p$, an estimate of the Navarro–Frenk–White (NFW) density concentration, and an estimate of the velocity anisotropies $\beta$. We find that differences between the potential and density NFW concentrations induce a $10\%$ bias in the caustic masses. We also find that large ($100\%$) systematic errors in the observed ensemble average velocity anisotropies and concentrations translate to small ($5\%$--$10\%$) biases in the inferred masses.

Key words: galaxies: clusters: general – galaxies: kinematics and dynamics

Online-only material: color figures

1. INTRODUCTION

Under Newtonian dynamics, the escape velocity is related to the gravitational potential of the system:

\[ v_{\text{esc}}^2(r) = -2\Phi(r). \] (1)

If the dynamics of the system are controlled by the gravitational potential, tracers that cannot escape the potential exist in a well-defined region of radius/velocity ($r$--$v$) phase space. The extrema of the velocities in this phase space define a surface, the escape-velocity profile, $v_{\text{esc}}(r)$, which can be observed in projected sky coordinates. Given the observed $v_{\text{esc}}(r)$, this “caustic” technique allows one to infer the mass profile of a cluster to well beyond the virial radius (Diaferio & Geller 1997).

With the latest deployments of wide-field ground-based multi-object spectrographs like VIMOS on the Very Large Telescope (VLT; Le Fèvre et al. 2003), IMACS on the Magellan (Dressler et al. 2011), and HECTOSpec\footnote{http://www.cfa.harvard.edu/mmt/hectospec} on the MMT, we are beginning to see large spectroscopic follow-up data sets of galaxy clusters. As a consequence, the caustic technique has become more widely adopted.

Geller et al. (2013, hereafter GMK) used the Millennium Simulation (Springel et al. 2005) to show that cluster-sized caustic masses within a projected $r_{200}$ (the radius which contains 200 times the critical density) are more precise and more accurate than virial masses measured from their projected velocity dispersions. However, the implementation of the escape-velocity technique employs a number of steps which result in biases in the inferred masses (Postman et al. 2012). Additionally of course, there are a variety of planned large-scale spectroscopy programs from both the ground (BigBoss\footnote{http://bigboss.lbl.gov/}) and from space (EUCLID\footnote{http://sci.esa.int/euclid}). These future efforts could enable caustic masses to be measured for many thousands of galaxy clusters. Gifford et al. (2013) used the Millennium Simulation to show that cluster-sized caustic masses within a projected $r_{200}$ (the radius which contains 200 times the critical density) are more precise and more accurate than virial masses measured from their projected velocity dispersions. However, the implementation of the escape-velocity technique employs a number of steps which result in biases in the inferred masses (Postman et al. 2012). Additionally of course, there are a variety of planned large-scale spectroscopy programs from both the ground (BigBoss\footnote{http://bigboss.lbl.gov/}) and from space (EUCLID\footnote{http://sci.esa.int/euclid}). These future efforts could enable caustic masses to be measured for many thousands of galaxy clusters.

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2. THEORY

Consider a mass distribution described by a spherical Navarro–Frenk–White (NFW) profile such that the mass density $\rho$ and the potential $\Phi$ radial profiles are

\[ \rho(r) = \frac{\rho_0}{(r/r_0)(1 + r/r_0)^2}, \]
\[ \Phi(r) = -\frac{4\pi G \rho_0 (r_0)^2 \ln(1 + r/r_0)}{r/r_0}. \] (2)

where $\rho_0$ is the normalization and $r_0$ is the NFW scale radius (Navarro et al. 1997). This is an example of a density–potential pair which share the same values for the shape parameters $\rho_0$ and $r_0$.
\[ \frac{dm}{dr} = 4\pi \rho(r)r^2, \]

\[ G \frac{dm}{dr} = -\Phi(r) \left( \frac{(r/r_0)^2}{1 + (r/r_0)^2} \ln(1 + r/r_0) \right), \tag{3} \]

where the unknowns are the gravitational potential \( \Phi(r) \) and the scale \( r_0 \). This is a key step in our escape-velocity technique, where we have equated the parameter \( \rho_0 \) in Equations (2). The NFW parameter \( \rho_0 \) sets the absolute scale for the mass density. The other NFW parameter \( r_0 \) defines the scale radius and is observable in projected data, assuming light traces mass.

We use Equation (1) to re-write Equation (3) as

\[ G M(<R) = \int_0^R \mathcal{F}(r) \nu_{\text{esc}}^2(r) dr, \tag{4} \]

where

\[ \mathcal{F}(r) = \frac{(r/r_0)^2}{1 + (r/r_0)^2} \ln(1 + r/r_0), \tag{5} \]

where the unknowns are the scale radius \( r_0 \) and the escape velocity \( \nu_{\text{esc}}^2(r) \), which is measured from the extrema in the radius and velocity \( r - v \) phase-space data.

More precisely, our estimate \( \mathcal{F}(r) \) should actually be

\[ \mathcal{F}(r) = -2\pi G \frac{\rho(r)r^2}{\Phi(r)}, \tag{6} \]

where \( \rho(r) \) and \( \Phi(r) \) are the spherically averaged density and potential profiles (see Diaferio & Geller 1997 or GMK).

The difference between \( \mathcal{F}(r) \) and \( \mathcal{F}(r) \) is that the former uses an exact profile for the densities and the potentials, while the latter assumes that only the density profile can be measured and that the potential has the same NFW shape parameters (i.e., concentration and scale) as the potential. We discuss whether or not this NFW-shape assumption holds in Section 3.1.

In projected data, we measure the velocities along the line of sight (l.o.s.), and so

\[ \langle \nu_{\text{esc}}^2(r) \rangle = \frac{1 - \beta(r)}{3 - 2\beta(r)} \langle \nu_{\text{esc}}^2(r) \rangle = (g(\beta(r)))^{-1} \langle \nu_{\text{esc}}^2(r) \rangle, \tag{7} \]

where the \( \beta \) is the standard velocity anisotropy parameter.

In the classical implementation of the caustic technique, the average \( \mathcal{F}_{\beta} \) is \( g(\beta(r)) \mathcal{F}(r) \) measured within N-body simulations and then applied to real data (Rines et al. 2013; Geller et al. 2013). In the literature, the average \( \mathcal{F}_{\beta} \) enters into the equation as being directly proportional to the mass, we must know it to high accuracy if escape-velocity masses are to be used in cosmological analyses.

A goal of this Letter is to drop the requirement that \( \mathcal{F}_{\beta} \) be calibrated from simulations. We assume that clusters are NFW density–potential pairs and apply Equation (4) directly. The unknowns \( r_0 \) and \( \langle \nu_{\text{esc}}^2(r) \rangle \) and \( \beta \) are constrained from observed data (Lin et al. 2004; Carlb erg et al. 1997; Wojtak & Łokas 2010; Budzynski et al. 2012; Diaferio & Geller 1997; Geller et al. 2013; Rines et al. 2013; Lemze et al. 2009; Biviano & Poggianti 2009; Host et al. 2009).

A final calibration in standard escape-velocity technique is that of the iso-density surface in \( r - v \) space which defines the average escape velocity, \( \langle \nu_{\text{esc}}^2(r) \rangle \). The density-weighted average escape velocity inside radius \( R \) is

\[ \langle \nu_{\text{esc}}^2(<R) \rangle = \frac{\int_0^R \rho(x) \nu_{\text{esc}}^2(x) dx}{\int_0^R \rho(x) dx} = -2\frac{\int_0^R \rho(x) \Phi(x) dx}{M(<R)}, \tag{8} \]

where we have used Equation (1). The integral in the numerator on the right-hand side of Equation (8) is twice the total potential energy of the system or \( 2W \) (Binney & Tremaine 1987), which leads to

\[ \langle \nu_{\text{esc}}^2(<R) \rangle = -\frac{4W(<R)}{M(<R)}, \tag{9} \]

where \( W \) and \( M \) are the total potential energy and mass of the system within the radius \( R \).

One often defines the following relation between the fraction of the total kinetic over the potential energy to that expected from a virialized halo:

\[ b = 1 + \frac{2T}{W}, \tag{10} \]

where \( T \) is the total kinetic energy. If we express the total kinetic energy of the system as \( T = 1/2M \langle v^2 \rangle \), Equation (9) becomes

\[ \langle \nu_{\text{esc}}^2(<R) \rangle = -\frac{4\langle v^2(<R) \rangle}{b - 1}, \tag{11} \]

where the average quantities are measured within the same radius, \( R \). The standard calibration assumes that \( b = 0 \) in a virialized and isolated halo such that \( 2T = -W \). Thus \( \langle \nu_{\text{esc}}^2 \rangle = 4\langle v^2 \rangle \), such that the escape-velocity phase-space surface is calibrated through a measurement of the velocity dispersion.

In this section, we have clarified where the calibration steps enter into the standard caustic analysis. The calibration includes the term \( \mathcal{F}_{\beta} \), which is directly proportional to the estimate of the mass. This term comprises two parts: \( \mathcal{F}(r) \) in Equation (6) and \( g(\beta(r)) \) in Equation (7). The other calibration step occurs from \( b \) in Equation (11), which decides the iso-density contour in the \( r - v \) phase space that defines the escape velocity. We have also presented a derivation of the caustic technique which does not require a calibration of \( \mathcal{F}_{\beta} \), but which assumes an NFW density–potential pair and uses the observables in Equation (4).

3. TESTING THE THEORY

We apply the caustic technique to 100 Millennium halos with masses \( M_{200} > 1 \times 10^{14} M_\odot h^{-1} \) and \( z < 0.1 \), where \( h = H_0/100 \) \( \text{km s}^{-1} \text{Mpc}^{-1} \). In three dimension, we use the particle positions and velocities. In the projected analyses, we use the Guo et al. (2011) semi-analytic galaxies within \( 30 h^{-1} \text{Mpc} \) of the halo centers projected along a random l.o.s. These volumes are large enough to incorporate realistic projection effects. The limits on the projected phase-space velocities are \( \pm 3000 \text{ km s}^{-1} \) relative to the halo velocity centroids, whereas the typical escape velocities are \( \sim 15000 \text{ km s}^{-1} \).

3.1. The NFW Shapes

In order to drop the N-body calibration of \( \mathcal{F}_{\beta} \), we assume that the NFW densities and potentials have the same parameters. This is expected if the matter distribution is concentric with the iso-potential surfaces (e.g., as in spherical symmetry; see also the classical potential solutions for homogeneous density.
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Figure 1. Comparison of the concentration measured via the density profile with \( c = r_{200}/r_0^\rho \) and the concentration measured via the potential profile with \( c = r_{200}/r_0^\Phi \). The blue line is unity and the green dashed line is the fit to the relationship with a slope = 0.89, intercept = 0.80. Error bars are 1 sigma uncertainties on the spherical NFW fits to the density and potential. (A color version of this figure is available in the online journal.)

distributions in Chandrasekhar 1969 and Binney & Tremaine 1987). However, Conway (2000) provides exact closed-form Newtonian potential solutions to an infinite family of heterogeneous spheroids and finds that the densities are generally not constant on the iso-potential bounding surfaces. In other words, while both the potential and density distribution could have the same general functional form like an NFW, they need not have identical shape parameters.

We compare the NFW density/potential shapes by first fitting the NFW density profile and determining \( \rho_0 \) and \( r_0 \) for each halo. The gravitational potentials are measured exactly through summation of \( Gm_i/r_i \) and then fit with an NFW using \( \rho_0 \) measured from the density, but allowing the potential scale parameter \( r_0 \) to be a free parameter.

In Figure 1, we compare the NFW concentrations \( c = r_{200}/r_0^\rho \), where \( r_{200} \) is the radius that contains a density corresponding to 200 \( \times \) the critical density. We find that the potentials have slightly higher concentrations than the densities. This difference suggests that our systems are not density–potential pairs that are simply related via spherical analytic solutions to the Poisson equation. Because of this, we expect that using Equation (4) will return an incorrect mass estimate due to its assumption of shape similarity in the density and potential profiles.

In Figure 2 we compare the three-dimensional (3D) escape-velocity masses with halo masses within \( r_{200} (M_{200}) \). In the
top left panel, we use the exact densities and potentials as measured using the particles (e.g., Equation (6)). These caustic mass estimates are nearly unbiased with a scatter of 13%. In the top right panel of Figure 2, we utilize Equation (4), where only the density profile is used to fit the 3D NFW concentrations and their errors. As expected from Figure 1, the NFW-inferred 3D caustic masses are biased low by ~10%. The scatter is 8%. The errors on this panel use a conservative uncertainty in $c = 50\%$.

A large uncertainty in the concentration has little effect on the scatter of the actual caustic mass estimate. This will become important when we discuss realistic observational biases and scatters in Section 3.3.

3.2. Virialization

It has been shown that the virial relation $2T = -W$ is often not met in simulated halos (Shaw et al. 2006; Bett et al. 2007; Neto et al. 2007; Davis et al. 2011). This does not mean that the system is not virialized, but simply that more terms from the tensor virial equation are required, usually in a surface pressure kinetic term. So the question then is at what radius do we begin to see a bias expected from Equation (11) when $\langle b \rangle \neq 0$?

To test this, we measure the exact (unbiased) caustic masses using $F(r)$ at 1, 0.9, 0.7, and 0.5 × the virial radius. We detect no appreciable bias until we reach half a virial radius where the masses become biased low by 10%. We calculate $\langle b \rangle = 0.1$ for particles within this radius. We then apply $\langle b \rangle = 0.1$ during the virial calibration stage of the caustic technique and find no mass bias. Serra et al. (2011) conduct a similar test, but against various fractions of their membership radius $R_{\text{Treu}}$, as opposed to an intrinsic cluster property like $R_{200}$. They find that there is a preferred radius of $0.7 \times R_{\text{Treu}}$. We come to a slightly different conclusion: the choice of radius does not matter, so long as the correct $\langle b \rangle$ is used. We also find that there is no bias when caustic masses are calibrated using data within $0.7 \leq R \leq 1.5R_{200}$.

3.3. Velocity Anisotropy

When the data are projected along the l.o.s., velocity anisotropies in the orbits of the galaxies must be taken into account (Diaferio & Geller 1997; GMK). In the bottom-left panel of Figure 2, we use $F_\beta(r)$ which is the exact $F(r)$ profile multiplied by the exact $\beta(r)$ profile. The increase in the scatter from the 3D (~10%) case to the l.o.s. (~25%) case is identical to what was measured in GMK, who use the classical caustic technique and a constant $F_\beta$. Therefore, for any given cluster, there is no gain in accuracy or precision in the estimated caustic masses by measuring a $\beta(r)$ profile for each cluster. The scatter is dominated by l.o.s. variations in the projected velocity dispersion (see also GMK).

We show our most realistic comparison of the caustic masses to $M_{200}$ in the bottom-right panel of Figure 2. Here we drop explicit knowledge of the concentrations and apply the ensemble average $\langle c \rangle = 5 \pm 2$ for every halo in $F(r)$ (see Figure 1). We also drop explicit knowledge of the anisotropy profile and instead use $\langle \beta \rangle = 0.2 \pm 0.2$, which is the average $\beta$ for these halos. Using these estimates, we find that the scatter is only slightly higher than in Figure 2 (bottom left). Large uncertainties in the average anisotropy and concentrations do not appreciably add scatter to what is already there from the l.o.s. projection. The bias in Figure 2 (bottom right) is caused by the faulty assumption that the halos have the same NFW density and potential concentrations (see Figure 1).

Systematic errors in the observable ensemble averages for the concentrations and the velocity anisotropies do impart mass biases. When we impose $\langle \beta \rangle = 0.0 \pm 0.2$, the average bias changes from $-10\%$ to $-18\%$, while $\langle \beta \rangle = 0.4 \pm 0.2$ results in an average mass bias of $+5\%$. When we impose $\langle c \rangle = 3 \pm 0.1$, the bias changes from $-8\%$ to $-13\%$, while $\langle c \rangle = 6 \pm 2$ results in a mass bias of $-7\%$. These average concentration values cover the full range of observational estimates in the literature (Carlberg et al. 1997; Lin et al. 2004; Wojtak & Łokas 2010; Budzynski et al. 2012).

4. CONCLUSIONS

One goal for this Letter was to test the fundamental statistical and systematic precision of the escape-velocity (or caustic) technique to measure masses of cluster-sized halos in N-body simulations. Given the 3D data, caustic masses are unbiased with 10%–15% precision (similar to or better than the virial scaling relation of Evrard et al. 2008). The scatter increases to 25% as a result of l.o.s. projections.

Our second goal was to re-frame the theory in terms of observable quantities and remove calibrations from N-body simulations. We utilized the weak assumption that the observed density and potential profiles can be described by an NFW with the same shape parameters, specifically the scale parameter $r_0$. We find that this latter assumption does not hold in the Millennium Simulation data, and the inferred cluster masses are biased low by ~10%. The virial calibration can also contribute to biases in the caustic masses when the velocity dispersion is averaged over a radius where the total binding energy is not represented by virial expectations. We show that large uncertainties in the ensemble average of the velocity anisotropies and concentrations do not contribute significantly to the intrinsic l.o.s. scatter in projected caustic masses. However, large (e.g., 100%) systematic errors in the average velocity anisotropies and concentrations can lead to additional 5%–10% biases in the caustic masses.

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