External-Field-Induced Phase Transformation and Associated Properties in a Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ Metamagnetic Shape Memory Wire

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Abstract: Metamagnetic shape memory alloys exhibit a series of intriguing multifunctional properties and have great potential for applications in magnetic actuation, sensing and magnetic refrigeration. However, the poor mechanical properties of these alloys with hardly any tensile deformability seriously limit their practical application. In the present work, we developed a Ni-Fe-Mn-In microwire that exhibits both a giant, tensile superelasticity and a magnetic-field-induced first-order phase transformation. The recoverable strain of superelasticity is more than 20% in the temperature range of 233–283 K, which is the highest recoverable strain reported heretofore in Ni-Mn-based shape memory alloys (SMAs). Moreover, the present microwire exhibits a large shape memory effect with a recoverable strain of up to 13.9% under the constant tensile stress of 225 MPa. As a result of the magnetic-field-induced first-order phase transformation, a large reversible magnetocaloric effect with an isothermal entropy change $\Delta S_m$ of 15.1 J kg$^{-1}$ K$^{-1}$ for a field change from 0.2 T to 5 T was achieved in this microwire. The realization of both magnetic-field and tensile-stress-induced transformations confers on this microwire great potential for application in miniature multi-functional devices and provides an opportunity for multi-functional property optimization under coupled multiple fields.

Keywords: metamagnetic shape memory alloy; microwire; superelasticity; martensitic transformation; magnetocaloric effect; magnetic-field-induced phase transformation; magnetostructural transformation; shape memory effect

1. Introduction

Shape memory alloys (SMAs), as a unique class of smart materials, which combine the functional properties such as shape memory effect (SME), superelasticity (SE) and elastocaloric effect, have drawn great attention in recent years [1,2]. The underlying mechanism of these properties is a reversible phase transformation between a high-temperature austenite phase and a low-temperature martensitic phase when an external stimulus of stress or temperature is applied [3]. Thus, SMAs show great potential for application as actuators and sensors in industrial [4,5], automotive [2,6], aerospace [3,7], micro-electromechanical system (MEMS) [8] and biomedical [9] fields. For the majority of actuators and sensors, fast response and large output strain/stress are imperative and desirable properties. Metamagnetic shape memory alloys (MMSMAs) have provoked much interest in recent years due to their high response frequency and output stress...
arising from the strong coupling of crystal and magnetic structures. In these alloys, it is possible to obtain such multifunctional properties as magnetic superelasticity [10,11], magnetic shape memory effect [12], magnetoresistance [13] and magnetocaloric effect [14–16].

In principle, MMSMAs can display a phase transformation under an external field of magnetic field, stress or temperature and optimized multifunctional properties can be anticipated under the coupling of magnetic field, stress and temperature. Unfortunately, polycrystalline MMSMAs show intrinsic brittleness, as a result of deformation and transformation incompatibility at grain boundaries and triple junctions [17], which severely limits their practical application. Moreover, it is difficult for these alloys to serve under the condition of the simultaneous application of magnetic field and stress in order to exhibit optimized multifunctional properties because they can easily fracture under external stress due to their high brittleness. It is of great importance to develop MMSMAs with good mechanical properties so that they can bear a high enough stress for stress-induced martensitic transformation.

Recently, it was proposed that the deformation and transformation incompatibility at grain boundaries and triple junctions in SMAs could be diminished by reducing their dimensions [18]. Low-dimension SMAs (particles, wires, films, ribbons, micropillars or foams) exhibit great application potential in micro-actuators or micro-sensors. This is due to the high ratio of surface to volume, which could improve the response speed [8,19]. The Taylor–Ulitzovsk [20,21] and melt-extraction [22] methods are two feasible and easy methods to produce magnetic shape memory microwires. The Taylor–Ulitzovsk method, which involves rapid solidification and drawing, is prone to produce microwires with an oligocrystalline structure. This structure reduces the incompatibility between different grains and thus effectively enhances the mechanical properties of Ni-Mn-based MMSMAs [23,24]. Although scattered attempts have been made to investigate the external-field-induced transformation of Ni-Mn-based MMSMA microwires that were prepared using this method, the reported microwires with a magnetic-field-induced transformation exhibit a limited recoverable strain of superelasticity and those with a large recoverable strain barely display magnetic-field-induced transformation. Therefore, there is an urgent need to develop high-performance MMSMAs with both a giant recoverable strain and a magnetic-field-induced first-order phase transition.

In the present work, we successfully developed a Ni-Mn-Fe-In MMSMA microwire exhibiting a giant, tensile superelasticity with a recoverable strain higher than 20%. Furthermore, the microwire shows a magnetic-field-induced first-order phase transformation and a reversible isothermal magnetic entropy change of 15.1 J kg⁻¹ K⁻¹ for a field change from 0.2 T to 5 T. The simultaneous achievement of a magnetic-field-induced phase transformation and a giant, tensile recoverable strain confers on this microwire great potential for application in miniature multifunctional devices.

2. Materials and Methods

Ni₈₃Mₐ₃FeₓIn₆₅ (at. %) polycrystalline button ingots were prepared by arc melting the pure Ni, Mn, Fe, and In elements. The ingots were melted four times in order to ensure homogeneity. The Taylor–Ulitzovsk method [20,21] was used to prepare the glass-coated microwires with a diameter of 50–150 μm. After removing the glass sheath, the microwires were tested without any post heat treatments. The cross-section and surface morphologies of the microwire were investigated using a scanning electron microscope (SEM, Carl Zeiss, Oberkochen, Germany). The crystallographic orientation was studied using electron backscatter diffraction (EBSD, Carl Zeiss, Oberkochen, Germany), which was conducted at room temperature in the SEM. Synchrotron high-energy X-ray diffraction (HEXRD) experiments were conducted using a monochromatic X-ray beam with a wavelength of 0.1173 Å at the 11-ID-C beam line of the Advanced Photon Source at the Argonne National Laboratory, USA.
Mechanical tests were conducted in tension using a dynamic mechanical analyzer (DMA, TA Instruments, New Castle, DE, USA) with a maximum load of 18 N equipped with a closed furnace. The stress–strain curves were measured by force control at a loading–unloading rate of 50 MPa/min. The force was measured by using a load cell with a high resolution (10^3 N). The strain was determined by cross-head displacement using a high-resolution linear optical encoder that has a displacement resolution of 1 nm. The total length and gauge length of the samples for mechanical tests were about 12.2 mm and 7.0 mm, respectively. Magnetization as a function of temperature (\(M(T)\)) under constant magnetic fields and magnetization as a function of magnetic field (\(M(H)\)) at constant temperatures were measured by a physical property measurement system (PPMS, Quantum Design, San Diego, CA, USA). The \(M(H)\) curves were measured by the standard loop process at different constant temperatures during two consecutive cycles of increasing the field to 5 T and then decreasing the field to 0 T. Before measuring the \(M(H)\) curves at each temperature, the microwire was cooled to 135 K. This temperature was held for 1 min and then increased to the test temperature. The mass of the samples for the \(M(T)\) and \(M(H)\) measurements was 1.41 mg.

3. Results
3.1. Microstructure and Crystal Structure

Figure 1a shows the cross-section morphology of the Ni_{50}Mn_{34}Fe_{13}In_{13} microwire, which indicates that the microwire had a regular, circular cross-section. The surface morphology of the Ni_{50}Mn_{34}Fe_{13}In_{13} microwire is displayed in Figure 1b, which demonstrates that the microwire had a smooth surface and uniform diameter. The EBSD orientation map of the Ni_{50}Mn_{34}Fe_{13}In_{13} wire was measured at room temperature and is shown in Figure 1c. No obvious grain boundaries can be observed in the sample used for EBSD measurement. This implies that the constraints of grain boundaries have been much reduced in the microwire—the grain size was as large as several millimeters [23].

![Figure 1](image)

**Figure 1.** Microstructure of the Ni_{50}Mn_{34}Fe_{13}In_{13} microwire at room temperature. (a,b) SEM images of the cross-section (a) surface (b); (c) Electron backscatter diffraction (EBSD) orientation map presented in inverse pole figure mode; the legend of a stereographic triangle (parallel to the wire axis direction AD) is also shown.

Figure 2a,b show the HEXRD patterns recorded at 298 K and 110 K, respectively, during the cooling of the Ni_{50}Mn_{34}Fe_{13}In_{13} microwire. The crystal structures of austenite and martensite were identified with the help of the software PowderCell [25]. The pattern
collected at 298 K in Figure 2a can be well indexed according to the cubic L2₁ Heusler structure (space group $Fm\bar{3}m$, No. 225) with lattice parameter $a_A = 5.970$ Å. As can be seen, besides the strong diffraction peaks of (220), (422) and (400), the superlattice reflections of (111), (311) and (331) can also be observed (see the inset of Figure 2a), which are characteristic of the L2₁ structure. At 110 K, the main diffraction peaks in Figure 2b can be well indexed according to the six-layered modulated (6M) structure of martensite (space group $P2/m$, No. 10) with lattice parameters $a_{6M} = 4.395$ Å, $b_{6M} = 5.622$ Å, $c_{6M} = 25.824$ Å and $\beta = 92.10^\circ$. However, several other small peaks can also be seen in Figure 2b. These small peaks can be well indexed according to the cubic L2₁ structure of austenite with lattice parameter $a_A = 5.955$ Å. This implies that a tiny amount of austenite was retained at this temperature.

Figure 2. High-energy X-ray diffraction (HEXRD) patterns recorded at the temperatures of (a) 298 K and (b) 110 K for the Ni₅₀Mn₃₄Fe₃In₁₃ microwire. The inset in (a) displays the magnified view of the pattern in the 2$\theta$ range of 1.5°–5.5°. “A” and “M” in the indices in (b) denote austenite and martensite, respectively.
Based on the geometric nonlinear theory of martensite, it is possible to evaluate the geometric compatibility between martensite and austenite. The middle eigenvalue $\lambda_2$ of the transformation stretch matrix $U$, which is used to characterize the geometric compatibility, can be computed with the algorithms reported in [26,27]. With the lattice parameters of austenite and martensite determined above, the $\lambda_2$ for the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire was determined to be 1.0083, which is close to 1. This implies a good geometric compatibility between martensite and austenite, which could explain the small thermal hysteresis of 8.9 K in the present microwire. This is because good geometric compatibility usually leads to a small thermal hysteresis [26].

3.2. Stress-Induced Phase Transformation and Superelasticity

In order to study the superelasticity that results from stress-induced martensitic transformation in the microwire, stress–strain curves at different constant temperatures were recorded. Figure 3a displays the tensile stress–strain curves at different constant temperatures in the temperature range of 213–283 K for the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire. The determination of the critical stress for stress-induced martensitic transformation $\sigma_{cr}$, stress hysteresis of the stress-induced martensitic transformation $\Delta \sigma$, irrecoverable strain after unloading $\varepsilon_{irr}$, superelastic strain $\varepsilon_{se}$ and elastic strain $\varepsilon_{el}$, is illustrated in Figure 3b. In Figure 3a, at 213 K, two stress plateaus can be observed during loading, which indicated that inter-martensitic transformation occurred at this temperature. An irrecoverable strain $\varepsilon_{irr}$ of 1.3% was observed after unloading when the maximum applied strain was 21.1%. This may be because a small amount of stress-induced martensite was stabilized and failed to transform back to austenite after unloading, as the test temperature (213 K) was slightly higher than the austenite transformation finish temperature $A_f$. This conjecture was confirmed by the recovery of the strain (1.3%) after heating to a higher temperature of 233 K. Encouragingly, the microwire exhibits excellent tensile superelasticity with almost no residual strain after unloading at higher temperatures (in the range between 233 and 283 K). Strikingly, a giant recoverable strain $\varepsilon_{re}$ of 20.3% was achieved in this temperature range, which is the highest recoverable strain reported so far in Ni-Mn-based SMAs. This value is much higher than that of Ni-Ti wire (approximately 11.5%), which is used for practical applications at present [28]. The temperature dependence of the critical stress for stress-induced martensitic transformation $\sigma_{cr}$ is shown in Figure 3c. It can be seen that the critical stress increased linearly with the increase of temperature at a rate of 1.69 MPa/K.

The shape memory effect was examined by load-biased thermal cycling tests under different constant stresses. The strain–temperature curves recorded under stress levels of 25, 75, 125 and 225 MPa for the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire are shown in Figure 4. The recoverable strain $\varepsilon_{re}$ and irrecoverable strain $\varepsilon_{irr}$ were determined and are illustrated in the figure. As can be seen, the strain associated with martensitic transformation was completely recovered after the cooling–heating cycle when the applied stresses were not higher than 75 MPa. The recoverable strains were high; they were 5.0% under 25 MPa and 8.9% under 75 MPa. The irrecoverable strain $\varepsilon_{irr}$ occurred when the stress increased to above 125 MPa. In spite of this, $\varepsilon_{re}$ continued to increase as the stress increased, and amounted to 9.5% under 125 MPa. Strikingly, when the stress increased to 225 MPa, a $\varepsilon_{re}$ as high as 13.9% was achieved. This is the highest shape memory strain that has been reported to date in Ni-Mn-based SMAs, which is of great importance to realizing a large stroke in actuator applications [2,29].
Figure 3. (a) Tensile stress–strain curves recorded at different constant temperatures in the range of 213–283 K for the Ni50Mn34Fe3In13 microwire. (b) Tensile stress–strain curve measured at 233 K with the determination of the following parameters: the critical stress for stress-induced martensitic transformation $\sigma_{cr}$, the stress hysteresis of the stress-induced martensitic transformation $\Delta\sigma$, the irrecoverable strain after unloading $\varepsilon_{irr}$, the superelastic strain $\varepsilon_{se}$ and the elastic strain $\varepsilon_{el}$. The total recoverable strain $\varepsilon_{rec}$ is the sum of $\varepsilon_{se}$ and $\varepsilon_{el}$. (c) Temperature dependence of the critical stress for stress-induced martensitic transformation $\sigma_{cr}$. 
3.3. Magnetic-Field-Induced Phase Transformation and Magnetocaloric Effect

In order to study the magnetic properties of the Ni₅₀Mn₃₄Fe₃In₁₃ microwire, the M(T) curves were measured. The M(T) curves measured under 0.05 T and 5 T are shown in Figure 5a. As can be seen, the high-temperature austenitic phase and low-temperature martensitic phase are ferromagnetic and weak magnetic, respectively. During cooling, a major part of the austenite transformed into martensite when the temperature range was: (1) between 184 K and 182 K under 0.05 T; and (2) between 164 K and 162 K under 5 T, respectively. Upon further cooling, the remaining austenite continuously and gradually transformed into martensite. The dM/dT as a function of temperature, which is derived from the M(T) curves in Figure 5a, is illustrated in Figure 5b. The martensitic transformation temperature (Tₘ) and the reverse transformation temperature (Tₐ) were determined by the temperatures corresponding to the maximum dM/dT values during cooling and heating, respectively. The Tₘ under the magnetic fields of 0.05 T and 5 T were 182.7 K and 162.2 K, respectively, while the Tₐ under 0.05 T and 5 T were 197.8 K and 178.3 K, respectively. As can be seen from Figure 5b, all the phase transformation temperatures decreased under 5 T when compared to those under 0.05 T. This may be due to the stabilization of austenite with a higher magnetization by the applied magnetic field. Specifically, Tₐ decreased by 19.5 K when the applied field was 5 T. Thus, the magnetic field dependence of Tₐ, ΔTₛ/μ₀ΔH, was ~3.94 K/T.

The change in transformation temperature (ΔTₛ) induced by the change in magnetic field (μ₀ΔH) usually follows the Clausius–Clapeyron relation [12,30,31]:

\[
\Delta T_s = \frac{\Delta M}{\mu_0 \Delta H} \Delta S_v.
\]

The transformation entropy change ΔSᵥ estimated from the endothermic peak of the reverse transformation from the differential scanning calorimetry curve (not shown here) is 18.1 J kg⁻¹ K⁻¹. The magnetization difference ΔM obtained from the M(T) curve under 5 T was 68.0 A m² kg⁻¹. Therefore, ΔM/ΔSᵥ is 3.76 K/T, which is consistent with the experimental value of ΔTₛ/μ₀ΔH (3.94 K/T). The obvious decrease in phase transformation temperatures indicated that a metamagnetic first-order phase transformation from...
martensite to austenite could be induced if a magnetic field was applied at a temperature that was close to the reverse transformation temperature.

To verify if the magnetic-field-induced phase transformation could occur in the Ni₅₀Mn₃₄Fe₃₅In₁₃ microwire and to examine the reversibility of the transformation, the M(H) curves at different temperatures were measured. The M(H) curves measured during two cycles of ascending and descending magnetic fields at different temperatures in the range 166–186 K are shown in Figure 5c. The thin lines and thick lines represent the first cycle and the second cycle of the ascending and descending magnetic fields, respectively. A rapid increase in magnetization was observed in the initial low-field range (below 0.2 T) at all the test temperatures. This may be due to the initial coexistence of weak magnetic martensite and a small amount of ferromagnetic austenite before the magnetic field was applied. As the magnetic field further increased, a jump in magnetization was observed at the critical field $\mu_0H_{cr}$, particularly in the temperature range 178–186 K. This phenomenon implies that a strong metamagnetic first-order phase transformation from weak magnetic martensite to ferromagnetic austenite can be induced by the magnetic field. It is worth mentioning that the critical field $\mu_0H_{cr}$ decreased as the temperature increased. Figure 5c indicates that only a portion of the phase transformation was induced under the magnetic field of 5 T at 166 K and 175 K. However, in the temperature range 178–186 K, the saturation of magnetization was observed at high fields. This indicates that the sample could transform completely into austenite at 5 T.
Figure 5. (a) \( M(T) \) curves measured under 0.05 T and 5 T for the Ni\(_{50}\)Mn\(_{34}\)Fe\(_{3}\)In\(_{13}\) microwire, (b) \( \frac{dM}{dT} \) derived from the curves in (a) shown as a function of temperature and (c) \( M(H) \) curves measured during the first (thin lines) and second (thick lines) cycles of ascending and descending magnetic fields at different constant temperatures for the Ni\(_{50}\)Mn\(_{34}\)Fe\(_{3}\)In\(_{13}\) microwire.
When comparing the first and second cycles of $M(H)$ curves, in the temperature range from 178 to 186 K, during increasing the magnetic field, the magnetization in the low-field region of the second cycle was slightly higher than that in the first cycle. This indicated that a small amount of austenite induced in first field cycle was retained and did not transform back into martensite during the decreasing magnetic field in the first cycle. The curve recorded during the decreasing field in the first cycle almost overlapped with that recorded during the decreasing field in the second cycle. In addition, the $M(H)$ curve recorded in the low magnetic field range during the increasing field in the second cycle was consistent with that during the decreasing field in the second cycle. These phenomena indicated that the part of retained austenite (only a tiny portion) after descending field in the first cycle did not participate in the subsequent transformation any more, and thus a reversible transformation between the martensite transformed back in the first cycle and the austenite could happen in the second and subsequent cycles. This is similar to the cases in [23,32]. As a result, a reversible first-order phase transformation, induced by a magnetic field, was achieved in the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire.

Magnetically driven multifunctional properties, such as magnetic superelasticity, magnetothermoelectricity, magnetoconductivity, and magnetocaloric effect, were anticipated in this Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire. This is based on the reversible first-order phase transformation that was induced by a magnetic field. The magnetocaloric effect was estimated as an example of the multifunctional properties mentioned above. The reversible magnetic-field-induced entropy change ($\Delta S_m$) was estimated from the $M(H)$ curves in Figure 5c. In the second cycle, the magnetic-field-induced phase transformation was reversible and, thus, the resultant $\Delta S_m$ was reversible as well. Therefore, the $M(H)$ curves in the second cycle were used to compute the reversible $\Delta S_m$.

The critical field $\mu_0H_c$ for magnetic-field-induced phase transformation, extracted from the $M(H)$ curves in the second cycle, is shown as a function of temperature in Figure 6a. Linear fitting of the $\mu_0H_c$ vs. $T$ data yielded a slope of $-0.237$ T/K, which was in accordance with the experimental $\mu_0\Delta H/\Delta T_c$ value ($-0.254$ T/K). As a tiny amount of austenite coexists with martensite before applying the magnetic field, the estimation of $\Delta S_m$ using the Maxwell relation may lead to spurious results [33]. In contrast, estimation using the Clausius–Clapeyron relation could yield the correct value of $\Delta S_m$ even in the case of the coexistence of two phases, since $\Delta S_m$ in the Clausius–Clapeyron relation is directly connected to the field-induced magnetization difference at any given temperature. Therefore, it is more suitable to use the Clausius–Clapeyron relation to estimate the reversible $\Delta S_m$. The $\Delta S_m$ can be estimated by the following relation [34–36]:

$$\Delta S_m = -\Delta M' \frac{d(\mu_0H_c)}{dT}$$  \hspace{1cm} (2)

in which $\Delta M'$ is the magnetization difference between the magnetization values at the final and initial fields. Since the magnetization rapidly changes in the $M(H)$ curves below 0.2 T, which could lead to numerical instabilities, the initial magnetic field selected was 0.2 T. The $d(\mu_0H_c)/dT$ is $-0.237$ T/K, as mentioned above.
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Figure 6. (a) Critical magnetic field for magnetic-field-induced phase transformation ($\mu_0 H_{cr}$) that was extracted from the $M(H)$ curves in the second cycle in Figure 5b, shown as a function of temperature for the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire. The dashed line represents the linear fitting of the data (denoted by symbols). (b) Reversible magnetic-field-induced entropy change $\Delta S_m$ as a function of temperature for the field change from 0.2 T to 5 T for the Ni$_{50}$Mn$_{34}$Fe$_{3}$In$_{13}$ microwire.

The reversible field-induced entropy change $\Delta S_m$ for a magnetic field change from 0.2 T to 5 T at different temperatures is displayed in Figure 6b. It can be seen that an inverse magnetocaloric effect was achieved as the $\Delta S_m$ values at all the temperatures are positive. The maximum reversible $\Delta S_m$ for a magnetic field change from 0.2 T to 5 T is as high as 15.1 J kg$^{-1}$ K$^{-1}$, which is higher than that in typical MMSMA microwires [23,33]. The large reversible magnetocaloric effect and high specific surface area confer on the present microwire high potential for magnetic refrigeration applications.

4. Discussion

The magnetostress is an important property for magnetic actuation applications and it is usually defined as the change in the critical stress for stress-induced martensitic transformation under a given magnetic field [37]. In Ni-Mn-based MMSMAs, since the
austenite is ferromagnetic and the martensite is weak magnetic, the magnetic field favors austenite. This leads to austenite stabilization and an increase in critical stress for stress-induced martensitic transformation at a given temperature; the magnetic field and the stress act in opposite directions under simultaneously applied magnetic field and stress.

The Zeeman energy, which arises from the difference between the saturation magnetizations of austenite and martensite, is the driving force for magnetic-field-induced first-order phase transformation [38]. Zeeman energy continuously increases with an increasing magnetic field. Therefore, it is possible to achieve a large output magnetostress in the present Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire, considering the large magnetization difference between austenite and martensite.

It is possible to predict the magnetostress as a function of applied field if the change in critical stress for stress-induced phase transformation with temperature ($\Delta \sigma/\Delta T$) and the change in transformation temperature with applied field ($\Delta T/\mu_0 \Delta H$) are known. The change in stress with applied magnetic field ($\Delta \sigma/\mu_0 \Delta H$) can be approximated as follows [37,38]:

$$\frac{\Delta \sigma}{\mu_0 \Delta H} = \frac{\Delta \sigma}{\Delta T} \times \frac{\Delta T}{\mu_0 \Delta H}. \quad (3)$$

The $\Delta \sigma/\Delta T$ and $\Delta T/\mu_0 \Delta H$ for the present Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire are 1.69 MPa/K and $-3.94$ k/T, respectively, as determined before. With Equation (3), $\Delta \sigma/\mu_0 \Delta H$ was estimated to be 6.66 MPa/T for the Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire. Therefore, a large magnetic work output is expected from the present microwire, showing its potential for magnetic actuation applications. Under a magnetic field of 1 T, it is possible to obtain a magnetostress of 6.66 MPa and under 5 T, the magnetostress would be 33.3 MPa.

The present Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire exhibited both magnetic-field-induced phase transformation and stress-induced martensitic transformation. Since stress-induced martensitic transformation occurred between 213 K and 283 K, a considerable elastocaloric effect was anticipated in this temperature range. Based on the magnetic-field-induced transformation, a large reversible magnetocaloric effect was achieved and other magnetoresponsive properties such as magnetic-field-induced strain and magnetoresistance were expected. Owing to the coupling between elastic deformation and magnetization, the elastomagnetic effect [39–41] could also be achieved in the microwire. Since the strain change could be detected by monitoring the change in magnetization, the microwire could also be used in non-contact strain sensors.

5. Conclusions

A Ni-Fe-Mn-In microwire exhibiting giant tensile superelasticity and magnetic-field-induced first-order phase transformation was developed. This Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire shows a giant recoverable strain of more than 20% as a result of stress-induced martensitic transformation in the temperature range of 233–283 K. This represents the highest recoverable strain reported heretofore in Ni-Mn-based SMAs. In addition, the present microwire exhibits a large shape memory effect with a recoverable strain of up to 13.9% under a constant tensile stress of 225 MPa. These properties contrast with those in the bulk MMSMAs that barely show any tensile deformability. Due to the considerable magnetization difference between martensite and austenite, magnetic-field-induced first-order phase transformation is realized in this microwire. Thus, a series of magnetoresponsive properties were anticipated. Indeed, a large reversible magnetocaloric effect, with an isothermal entropy change $\Delta S_m$ of 15.1 J kg$^{-1}$ K$^{-1}$ for a field change from 0.2 T to 5 T, was obtained from this microwire. The achievement of magnetic-field and stress-induced transformations confers on this Ni$_{50}$Mn$_{34}$Fe$_3$In$_{13}$ microwire great potential for application in miniature multifunctional devices.
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