First-Principles Simulations of Warm Dense Lithium Fluoride

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We perform first-principles path integral Monte Carlo (PIMC) and density functional theory molecular dynamics (DFT-MD) calculations to explore warm dense matter states of LiF. Our simulations cover a wide density-temperature range of $2.08 - 15.70 \text{ g cm}^{-3}$ and $10^3 - 10^9 \text{ K}$. Since PIMC and DFT-MD accurately treat effects of atomic shell structure, we find a pronounced compression maximum and a shoulder on the principal Hugoniot curve attributed to K-shell and L-shell ionization. The results provide a benchmark for widely-used EOS tables, such as SESAME, LEOS, and models. In addition, we compute pair-correlation functions that reveal an evolving plasma structure and ionization process that is driven by thermal and pressure ionization. Finally, we compute electronic density of states of liquid LiF from DFT-MD simulations and find that the electronic gap can remain open with increasing density and temperature to at least $15.7 \text{ g cm}^{-3}$.

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I. INTRODUCTION

Progress in our understanding of warm dense matter (WDM) relevant to fusion energy and astrophysical phenomena relies on the development of accurate techniques to determine the equation of state (EOS) of materials across wide density-temperature regimes. The EOS provides well-defined thermodynamic states that can be measured experimentally in dynamic shock experiments and further used for hydrodynamic modeling of experiments. The state of a shock in dynamic compression experiments is often measured with impedance matching techniques via an optically transparent interferometer window. While there are several materials used for shock windows (quartz, diamond, MgO, etc), LiF is frequently used because it has several favorable optical and structural properties under compression.

Numerous shock experiments have been performed to characterize the EOS, optical, and mechanical properties of LiF in order to optimize its use as an interferometer window. The shock Hugoniot curve has been measured up to 14 Mbar. Experimental data has indicated that the large LiF optical gap ($\sim 12 \text{ eV}$) decreases with compression to 800 GPa, and, upon extrapolation, closes above 4000 GPa. In contrast, recent first-principles simulations indicate that the optical gap should increase with density to at least 500 GPa. Despite this discrepancy, there is agreement between experiment and theory that the refractive index increases linearly with density up to 800 GPa. In addition, the EOS of LiF has been measured in diamond anvil experiments. From these investigations, it is known that LiF has a high melting temperature ($\sim 3000 \text{ K}$ at 1 Mbar) and remains in the B1 structural phase up to at least 1 Mbar, which makes LiF an excellent window material in shock wave experiments. Additionally, ultrasonic measurements have been used to measure elastic moduli.

Many theoretical investigations have also aimed to

FIG. 1: (a) Comparison of PIMC/DFT-MD shock Hugoniot curves with SESAME-7271, LEOS-2240, and the Purgatorio (Lynx-2240) model, as well as previous DFT-MD and experiments in $P$-$\rho$ space. The PIMC/DFT-MD Hugoniot curves are plotted for four initial densities, corresponding to 1–1.3-fold of ambient density. PIMC/DFT-MD and Purgatorio treat the quantum-mechanical shell structure of the ions and, thus, reveal a pronounced compression maximum and a shoulder due to K-shell and L-shell ionization effects. The SESAME and LEOS EOS tables are derived from models that do not explicitly treat shell effects. Plots (b) and (c) show a zoom in of the regions near the experimental data and the compression maximum, respectively.
FIG. 2: Temperature-pressure conditions for the PIMC and DFT-MD calculations along four isochores corresponding to the densities of 2.082, 3.651, 7.582, and 15.701 g cm$^{-3}$. The blue, dash-dotted line shows the Hugoniot curve for an initial density of $\rho_0 = 2.635$ g cm$^{-3}$.

understand the EOS, electronic, and optical properties of LiF. Most of these simulations focus on relatively low-pressure and low-temperature regimes to help constrain the phase, melt, and optical properties that are important for shock window experiments. The highest temperature and pressure simulations at which LiF has been studied so far, using density functional theory molecular dynamics (DFT-MD) methods, were performed by Clérouin et al. $^{10}$, which predicted the EOS and shock Hugoniot curve up to a density of 7 g cm$^{-3}$ (14 Mbar) and a temperature of 47,000 K $^{10}$.

Because of the relevance of LiF for shock physics, it is desirable to have a first-principles EOS derived for much higher temperature and density conditions that span the condensed matter, warm dense matter, and plasma physics regimes as a reference for shock experiments and hydrodynamic simulations. In recent works, we have developed a first-principles framework to compute coherent EOSs across a wide range of density-temperature regimes relevant to WDM by combining results from state-of-the-art path integral Monte Carlo (PIMC) and DFT-MD methods for first-row and second-row elements. In this paper, we apply our PIMC and DFT-MD methods to compute the EOS and plasma properties of LiF across a much larger density-temperature range than has been studied in previous first-principles studies. We also study the evolution of the plasma structure, ionization, and density of states over the WDM regime. And, finally, we compare our PIMC/DFT-MD shock Hugoniot curves with widely-used models and experiments.

The paper is organized as follows: Sec. II describes the simulation methods. Section III provides the internal energy and pressure EOS. Section IV discusses the shock Hugoniot curves. Section V characterizes the plasma structure evolution and ionization processes as a function of temperature and density via pair-correlation functions. Section VI analyzes the electronic density of states as a function of LiF density and pressure, and, finally, Sec. VII summarizes our work.

II. SIMULATION METHODS

Rigorous discussions of the PIMC and DFT molecular dynamics (DFT-MD) methods have been provided in previous works, and the details of our simulations have been presented in our previous publications. Here, we summarize the methods and provide the simulation parameters specific to LiF.

The general idea of our approach is to perform simulations along isochores at high temperatures ($T > 1 \times 10^6$ K).
using PIMC and at low temperatures (T ≤ 1×10^6 K) using DFT-MD. We show the two methods produce consistent results at overlapping temperature regimes. The PIMC method samples the space of all quantum particle paths to determine the thermal density matrix of the many-body system. PIMC increases in efficiency with temperature (scaling as 1/T) as quantum paths become shorter and more classical in nature. In contrast, DFT-MD becomes increasingly inefficient with increasing temperature, as the number of occupied bands increases unfavorably with temperature (scaling roughly as ∼T^{3/2}). The only uncontrolled approximation in PIMC is the use of the fixed-node approximation, which restricts paths to avoid the well-known fermion sign problem. We have shown the associated error is small for relevant systems at high enough temperatures. The main approximation in DFT-MD is the use of an approximate exchange-correlation (XC) functional, though at temperatures relevant to WDM, error in the XC is small relative to the total energy, which is the important quantity for EOS and Hugoniot simulations.

PIMC uses a small number of controlled approximations, whose errors can be minimized by converging parameters, such as the time step and system size. In simulations using free-particle nodes, we typically use a time-step of 1/256 Ha⁻¹ for temperatures below 4×10^6 K, where the total energy per atom is converged within 1%. This results in using between 4 and 162 time slices for the temperature range studied with PIMC (0.5×10^6 to 1.034×10^9 K). Regarding finite size errors, we showed simulations of 8- and 24-atom cubic cells provide internal energies that agree within 1.0% and pressures that agree within 0.5% over the relevant temperature range for PIMC (T > 1×10^6 K). Our results for the internal energy and pressure typically have statistical errors of 0.3% or less.

We employ standard Kohn-Sham DFT-MD simulation techniques for our low temperature (T ≲ 1×10^6 K) calculations of warm dense LiF. Simulations are performed...
FIG. 6: Comparison of shock Hugoniot curves in P-$\rho/\rho_0$ space for various materials initialized at ambient or experimental densities. The initial densities (in g cm$^{-3}$) are He: 0.124, C: 2.253, N 0.807, O: 0.667, LiF: 2.635, Ne: 1.507, and Si: 2.329.

with the Vienna Ab initio Simulation Package (VASP)\textsuperscript{76} using the projector augmented-wave (PAW) method\textsuperscript{77,78}, and a NVT ensemble, regulated with a Nosé thermostat. Exchange-correlation effects are described using the Perdew-Burke-Ernzerhof\textsuperscript{79} generalized gradient approximation. Electronic wave functions are expanded in a plane-wave basis with a energy cut-off as high as 4000 eV in order to converge total energy. Size convergence tests up to a 64-atom simulation cell at temperatures of 10,000 K and above indicate that internal energies are converged to better than 0.1% and pressures are converged to better than 0.6%. We find, at temperatures above 250,000 K, 8-atom supercell results are sufficient for both energy and pressure since the kinetic energy far outweighs the interaction energy at such high temperatures\textsuperscript{80}. The number of bands in each calculation were selected such that orbitals with occupation as low as 10$^{-4}$ were included, which requires up to 7,500 bands in a 24-atom cell at 1×10$^6$ K. All simulations are performed at the Γ-point of the Brillouin zone, which is sufficient for high temperature fluids, converging total energy to better than 0.01% compared to a grid of k-points.

III. EQUATION OF STATE RESULTS

In this section, we report our combined PIMC and DFT-MD EOS results for the liquid, WDM, and plasma regimes at several densities in the range of 2.082–15.701 g cm$^{-3}$ and temperatures ranging from 10$^4$–10$^9$ K. The full-range of our EOS data is shown in pressure-density space in Fig. 1 and in temperature-pressure space in Fig. 2. These two figures will be discussed more thoroughly in Section VI. The Supplemental Material\textsuperscript{80} provides a table of our full EOS data set. In order to put the PAW-PBE pseudopotential energies on the same scale as all-electron calculations, we shifted all of our VASP DFT-MD energies by -107.061113 Ha/LiF. This shift was determined by performing isolated, all-electron atomic calculations with the OPIUM code\textsuperscript{81} and corresponding isolated-atom calculations using the appropriate pseudopotential in VASP.

In order to analyze the behavior of our EOS data, Figs. 3 and 4 compare pressure and internal energy, respectively, along four isochores from PIMC, DFT-MD, and the classical Debye-Hückel plasma model\textsuperscript{75} as a function of temperature. The pressures, $P$, and internal energies, $E$, are plotted relative to a fully ionized Fermi gas of electrons and ions with pressure, $P_0$, and internal energy, $E_0$, in order to compare only the excess pressure and internal energy contributions that result from particle interactions. With increasing temperature, the pres-
sure and internal contributions due to interactions gradually decrease from the strongly-interacting condensed matter regime, where bound states dominate, to the weakly-interacting, fully-ionized plasma regime, where agreement is found with the Debye-Hückel model. As one expects, the classical Debye-Hückel model becomes inadequate for lower temperatures ($T < 5 \times 10^6$ K) since it fails to treat bound electronic states. While the range of temperatures over which PIMC EOS data is needed to fill the temperature gap between DFT-MD and Debye-Hückel (roughly $2 \sim 5 \times 10^6$ K) is relatively small compared to the entire temperature range of the high energy density physics regime, this temperature range encompasses the important process of K-shell ionization, which is precisely where the full rigor of PIMC is needed to acquire an accurate EOS table.

The two figures together provide a coherent EOS over wide density-temperature range for LiF due to the fact that PIMC and DFT-MD provide consistent, overlapping results, with a maximum difference of 3% in the pressure and 3.6% ($\sim 1.7$ Ha/LiF) in the internal energy at $1 \times 10^6$ K. Furthermore, this agreement between PIMC and DFT-MD provides validation for the use of zero-temperature exchange correlation functionals in WDM applications and the use of free-particle nodes in PIMC. However, as noted by Karasiev et al., this may only be true when the total energy is large relative to the exchange-correlation energy. Finite-temperature exchange-correlation contributions were predicted to be significant for other properties, such as conductivity at low densities. At lower temperatures, PIMC results become inconsistent with DFT-MD results because the free-particle nodal approximation in PIMC simulations is no longer appropriate.

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**FIG. 8:** Pair-correlation functions of Li nuclei computed with PIMC simulations of LiF over a wide range of temperatures. Functions are compared for densities of (a) 2.082 and (b) 15.701 g cm$^{-3}$ (8-atom simulation cells).

**FIG. 9:** Pair-correlation functions of F nuclei computed with PIMC simulations of LiF over a wide range of temperatures. Functions are compared for densities of (a) 2.082 and (b) 15.701 g cm$^{-3}$ (8-atom simulation cells).

**FIG. 10:** Pair-correlation functions of Li-F nuclei computed with PIMC simulations of LiF over a wide range of temperatures. Functions are compared for densities of (a) 2.082 and (b) 15.701 g cm$^{-3}$ (8-atom simulation cells).
IV. SHOCK COMPRESSION

Dynamic shock compression experiments allow one to directly measure the equation of state and other physical properties of hot, dense fluids. Such experiments are often used to determine the principal Hugoniot curve, which is the locus of final states that can be obtained from different shock velocities. Density functional theory has been validated by experiments as an accurate tool for predicting the shock compression of a variety of different materials.\textsuperscript{82-84}

During a shock wave experiment, a material whose initial state is characterized by an internal energy, pressure, and volume, \((E_0, P_0, V_0)\), will change to a final state denoted by \((E, P, V)\) while conserving mass, momentum, and energy. This leads to the Rankine-Hugoniot relation\textsuperscript{85}

\[
(E - E_0) + \frac{1}{2}(P + P_0)(V - V_0) = 0. \tag{1}
\]

Here, we solve this equation for our computed first-principles EOS data set, which is reported in the Supplemental Material\textsuperscript{182}. We obtain a continuous Hugoniot curve by interpolating the EOS data with a rectangular bivariate spline as a function of \(\rho\) and \(T\). We have compared several different spline algorithms and find the differences are negligible given that reasonable choices are made for the isochore densities with respect to Hugoniot features. In order to obtain the principal Hugoniot curve, we used initial conditions based on the energy and pressure of ambient, solid LiF in the B1 phase computed with static DFT \((P_0 = 3.323 \text{ GPa}, E_0 = -107.417375 \text{ Ha}/\text{LiF}, V_0 = 16.346636 \text{ Å}^3/\text{LiF}, \rho_0 = 2.635 \text{ g cm}^{-3})\). The resulting Hugoniot curve has been plotted in \(P-\rho\) space in Fig. 1 in \(T-P\) space in Fig. 2 and in \(T-\rho/\rho_0\) space in Fig. 5.

Samples in shock wave experiments may be precompressed inside of a diamond anvil cell before the shock wave is launched in order to reach much higher final densities than are possible with a sample at ambient conditions.\textsuperscript{86,87} This technique allows shock wave experiments to probe a density-temperature regimes consistent with planetary and stellar interiors. Therefore, we repeat our Hugoniot calculation starting with initial densities of 1.1-1.3-fold of the ambient density.

Fig. 1 shows the temperature along the Hugoniot curve as a function of the shock-compression ratio for the principal Hugoniot curve and a curve corresponding to 1.3-fold precompression. Consistent with our studies of other elements, we find that an increase in the initial density leads to a slight reduction in the shock compression ratio because particles interact more strongly at higher density. In the high-temperature limit, all curves converge to a compression ratio of 4, which is the value of a non-relativistic, ideal gas. We also show the magnitude of the relativistic correction to the Hugoniot in the high-temperature limit. The shock compression and structure along the Hugoniot is determined by the excitation of internal degrees of freedom, such as dissociation and ionization processes, which increases the compression, and, in addition, the interaction effects, which decrease the compression.\textsuperscript{88}

In the structure of the principal Hugoniot curve, we identify a pronounced compression maximum at high temperature and a shoulder at lower temperature, which correspond to the ionization of the K-shell and L-shell in LiF. The lower-temperature shoulder on the principal Hugoniot curve occurs near a compression ratio of \(\rho/\rho_0 = 4.28\) and a temperature of \(9.00 \times 10^6 \text{ K}\) (77.56 eV), which corresponds to the K-shell ionization of lithium and the L-shell ionization of fluorine. The K-shell ionization energies of lithium are 75.64 eV (8.78 \(\times 10^6 \text{ K}\)) and 122.45 eV (1.42 \(\times 10^8 \text{ K}\)).\textsuperscript{89} The 2p state of lithium is already ionized by a temperature of 5.39 eV (6 \(\times 10^4 \text{ K}\)). The L-shell ionization energies of fluorine range from 17.42–185.19 eV (13, where charge density around the nuclei is reduced over the range of 1-8 \(\times 10^6 \text{ K}\). Propagating errors from our equation of state data into the Hugoniot curve shows that the statistical uncertainty in the density along the

![Comparison of nuclear pair-correlation functions computed with PIMC and DFT-MD for LiF at a temperature of 1 \(\times 10^6 \text{ K}\) and a density of 15.701 \(\text{ g cm}^{-3}\) (24-atom simulation cells).](image)
PIMC. We note that the classical Debye-Hückel model is limited to fill a relatively small gap in temperature (2-10 K), and PIMC results are plotted for higher temperatures.

The SESAME and LEOS Hugoniot curves provide good overall agreement with PIMC in this case, they do not exhibit any compression maximum related to shell structure. On the other hand, the DFT-based, average-atom Purgatorio (Lynx-2240) model does compute the shell structure for an average of multiple ionic states. Thus, Purgatorio predicts the correct ionization features, a shoulder and a well-defined compression maximum, along the principal Hugoniot curve in good agreement with PIMC. However, overall the Purgatorio Hugoniot curve is slightly less compressible than the PIMC prediction. Remarkably, Purgatorio achieves this level of accuracy while being 100-1000× more efficient than Kohn-Sham DFT-MD and PIMC. We note that the classical Debye-Hückel model is excellent agreement with PIMC for temperatures above 5×10^6 K. This means that for LiF, PIMC is only needed to fill a relatively small gap in temperature (2×10^6 K and 5×10^6 K) between DFT-MD and Debye-Hückel EOS data, which encompasses the K-shell compression peak.

We also compare with experimental data in Fig. 4 and Fig. 5 which is available for low temperatures and pressures. At lowest temperatures in Fig. 5, the Hugoniot curves of all models lie slightly above the shock melting measurement by Kormer et al. In Fig. 4 all models agree reasonably well with the experimental shock data of the Li and F nuclei. Therefore, we see that, while the SESAME and LEOS Hugoniot curves for other first- and second-row materials (4.596-fold compression) are computed with DFT-MD simulations in 64-atom cells at four densities. We plot the g(r) functions as a function of r/r_s, where r_s=(3/(4πn_e))^{1/3} and n_e is the electron number density of LiF, in order to clearly differentiate between correlation- and density-driven changes. The results we find are in a good agreement with trends found by Clérouin et al., but investigated for a larger density range. As in most fluids, LiF becomes more structured with increasing density. We also note that higher temperatures always result in less structured fluid at each density. Compared to the other g(r) functions, there is less structure in Li-Li curves, which implies those nuclei interact weakly. By examining the mean square displacements as a function of time, we also find the lithium atoms diffuse much faster due to their lighter mass. The fluorine atoms exhibit increasing strong correlations with density, preserving an ionic fluid structure, as seen in the F-F g(r) peak. Furthermore, the lithium atoms remain strongly correlated with ionic fluorine structure due to Coulomb interactions, as seen in the Li-F g(r) peak.

V. PAIR-CORRELATION FUNCTIONS

In this section, we provide a discussion of the temperature and density dependence of pair-correlation, g(r), functions and ionization processes in warm dense LiF. The radial pair correlation function is defined as

\[ g(r) = \frac{V}{4\pi r^2 n^2} \left( \sum_{j>i} \delta(r-r_{ij}) \right), \]

where N is the total number of particles, V is the cell volume, and r is the distance from the ith reference particle.

Fig. 7 shows Li-Li, Li-F, and F-F pair-correlation curves at a fixed, low temperature of 2×10^4 K computed with DFT-MD simulations in 64-atom cells at four densities. We plot the g(r) functions as a function of r/r_s, where r_s=(3/(4πn_e))^{1/3} and n_e is the electron number density of LiF, in order to clearly differentiate between correlation- and density-driven changes. The results we find are in a good agreement with trends found by Clérouin et al., but investigated for a larger density range. As in most fluids, LiF becomes more structured with increasing density. We also note that higher temperatures always result in less structured fluid at each density. Compared to the other g(r) functions, there is less structure in Li-Li curves, which implies those nuclei interact weakly. By examining the mean square displacements as a function of time, we also find the lithium atoms diffuse much faster due to their lighter mass. The fluorine atoms exhibit increasing strong correlations with density, preserving an ionic fluid structure, as seen in the F-F g(r) peak. Furthermore, the lithium atoms remain strongly correlated with ionic fluorine structure due to Coulomb interactions, as seen in the Li-F g(r) peak.

Figures 8 and 10 show ion-ion g(r) curves for Li-Li, F-F, and Li-F pairs in LiF plasmas, respectively. The g(r) functions were computed with PIMC at temperatures relevant to WDM for four densities. We first note that g(r) curves corresponding to heavier ions are...
systematically found further apart than lighter ions due to stronger Coulomb repulsion and Pauli exclusion from bound electrons. In each case, the atoms are kept farthest apart at low temperatures. As temperature increases, kinetic energy of the nuclei increases, leading to stronger collisions and making it more likely to find them at close range. At the same time, the atoms become increasingly ionized, which gradually reduces the Pauli repulsion, while increasing the ionic Coulomb repulsion. At the highest temperatures, the system approaches the Debye-Hückel limit, behaving like a weakly correlated system of screened Coulomb charges. As density increases, the likelihood of finding two nuclei at close range rises only slightly.

In order to show that PIMC and DFT-MD predict similar plasma structures, Fig. 11 compares Li-Li, Li-F, and F-F g(r) curves using both methods at $1 \times 10^6 K$ at our highest isochore density of $15.701 \text{ g cm}^{-3}$ in 24-atom simulation cells. The fact that the PIMC and DFT-MD g(r) curves nearly overlap indicates that both methods predict a consistent ionic plasma structure in addition to a consistent EOS. There are some small differences in the Li-Li g(r) DFT-MD and PIMC curves likely due to frozen-core pseudopotentials and exchange correlation effects.

Figs. 12 and 13 show the integral of the nucleus-electron pair correlation function, \( N(r) \), for Li-e and F-e in LiF plasma, respectively, as a function of temperature and density. \( N(r) \) represents the average number of electrons within a sphere of radius \( r \) around a given nucleus.

\[ N(r) = \left\langle \frac{1}{N_I} \sum_{e,i} \theta(r - |\vec{r}_e - \vec{r}_i|) \right\rangle, \]

where the sum includes all electron-ion pairs and \( \theta \) represents the Heaviside function.

In each figure, we compare our PIMC \( N(r) \) curves with the 1s ground-state of a corresponding isolated Li or F atom to gauge the extent of ionization. It is clear from Fig. 12 that the lithium ion is almost fully ionized for all temperatures and densities considered. While there are some partially bound states remaining in the lithium ions at a temperature of $1 \times 10^6 K$, by $8 \times 10^6 K$ the Li atoms have been fully ionized. In contrast, from Fig. 13 it is clear that the higher-Z, fluorine ion still has bound 1s electrons at $1 \times 10^6 K$ due to a higher binding energy. As temperature increases, the K-shell of the fluorine ions gradually becomes more ionized, causing \( N(r) \) to decrease. As density increases, it is apparent that higher temperatures are required to fully ionize the fluorine ion. Thus, we observe that the 1s ionization fraction decreases with density, which indicates that pressure ionization of the fluorine K-shell is absent, as we have observed for other first- and second-row elements in our previous work\(^{68,91}\).

Fig. 14 shows electron-electron pair correlations in LiF plasma for electrons having opposite spins. The functions are multiplied by the mass number density \( \rho \), so that the integral under the curves is proportional to the number
FIG. 14: The electron-electron pair-correlation functions for electrons with opposite spins in PIMC calculations of LiF plasma. Results are compared for densities of (a) 2.082 and (b) 15.701 g cm\(^{-3}\) at four temperatures (8-atom cells).

Fig. 14 shows electron-electron pair correlations in LiF plasma for electrons with parallel spins. The positive correlation at intermediate distances (\(r \approx 0.2\) Å) reflects that different electrons with parallel spins are bound to a given nucleus. For short separations, electrons strongly repel due to Pauli exclusion and the functions decay to zero. As density increases, the peak at intermediate distances decreases and clearly shows the effect of pressure ionization of the L shell. Pressure ionization is expected for L-shell orbitals because they are much larger than the K-shell orbitals and are therefore subject to Pauli exchange with nearby nuclei. As temperature increases, electrons become less bound, which also causes the correlation to become more like an ideal fluid.

VI. ELECTRONIC DENSITY OF STATES

In this section, we report DFT-MD results for the electronic density of states (DOS) as a function of temperature and density in the liquid and plasma states of LiF. This analysis provides further insight into the temperature-density evolution of ionization effects and the band gap. All DOS curves were computed with 64-atom simulation cells. At this cell size and temperature range (\(1 \times 10^4 - 5 \times 10^5\) K), we found a single k-point provides sufficiently converged DOS results. Smooth curves were obtained by averaging over a MD simulation and applying a Gaussian smearing of 0.5 eV to the band energies. Furthermore, the eigenvalues of each snapshot were shifted so that the Fermi energies, \(E_F\), align at zero, and the integral of the occupied DOS is normalized to 1.

Fig. 15 shows the total and occupied DOS at six points along the liquid and plasma shock Hugoniot curve as predicted by DFT-MD (see Section VI). At low temperatures and densities, the general structure is composed of three peaks below the Fermi energy, representing the atomic 1s, 2s and 2p states. The 1s peak is due to lithium, which is treated with an all-electron pseudopotential, while the fluorine pseudopotential has a frozen 1s core. Depending on the temperature-density conditions, the DOS exhibits a gap or pseudogap followed by a continuous spectrum of conducting states. The lowest density-temperature condition exhibits a gap, which is consistent with the work of Clérouin et al., who showed a gap in the liquid persists along the Hugoniot curve to the melting point over density range of 4.5–6.5 g cm\(^{-3}\). The DOS at higher temperature-density conditions exhibits a pseudogap, whose depth generally decreases for increasing temperature-density conditions along the Hugoniot. The DOS peaks broaden and merge at higher temperatures and densities as LiF becomes further ionized. For the highest temperature and density, the total DOS begins to resemble that of an ideal fluid.
FIG. 16: Electronic DOSs plotted at temperature-density conditions along the principal shock Hugoniot curve. The upper panel shows the total DOS (all), while the lower panel shows occupied DOS (occ).

Regarding the occupied DOS, the fraction of occupied states lying above the Fermi energy drastically increases as temperature-density conditions increase along the Hugoniot curve. Consistent with our pair-correlation analyses, we attribute the increase in occupation above the Fermi energy to a combination of thermal and pressure ionization. For lithium ions, both L-shell and K-shell states undergo a significant thermal ionization, while for fluorine ions, only the L-shell states are subject to thermal ionization in the temperature range considered for the DOS. The L-shell states in both lithium and fluorine are partially pressure ionized at the highest densities considered here, but 1s states remain bound for the conditions considered in the DOS plot.

Fig. 17 shows a set of DOS curves for a fixed temperatures as a function of density for off-Hugoniot states lying in the low-temperature liquid regime. While all curves shown are found to be liquid in the DFT-MD simulations, we note that any lower temperatures than those shown resulted in a frozen structure using 64-atom simulation cells. In this temperature-density regime, we find that the band gap forms at increasingly higher temperatures with increasing density. Based on our ionic pair correlation analysis in Fig. 4, we find the reason for this trend in the band gap is due to ordering maintained within the fluid due ionic Coulomb interactions. While higher temperatures tend to disorder the fluid, closing the gap, higher densities stabilize an ionic structure that promotes a gap. We also note that, for the low temperatures and high densities, it is clear that the K-shell states are not pressure ionized even at the highest density studied here (15.7 g cm$^{-3}$) and the majority of occupied states still lie below the Fermi energy.

VII. CONCLUSIONS

In this paper, we have extended the first-principles EOS of LiF to a much wider temperature-density range than it has ever been studied previously. For the first time, we are able to predict the compression maximum on the principal Hugoniot from first principles. We used PIMC and DFT-MD to construct a coherent EOS that bridges the liquid, WDM, and plasma regimes. We
showed that both PIMC and DFT-MD produce consistent EOS data in the range of $5 \times 10^5$–$1 \times 10^6$ K, validating the use of free-particle nodes in PIMC and zero-temperature XC functionals in DFT-MD for warm dense LiF. We then studied pair-correlations of electron and nuclei in LiF liquid and plasmas, revealing an evolving plasma structure and ionization process that is driven by thermal and pressure ionization effects. In addition, we computed the density of states to show how LiF can maintain an open band gap to densities as high as 15 g cm$^{-3}$ due to strong ionic correlations. Finally, we examined the shock compression behavior of LiF and computed a first-principles benchmark of the principal Hugoniot for several pre-compression conditions. We compare our PIMC Hugoniot results with widely used Thomas-Fermi-based models (SESAME and LEOS), which do not include shell effects, and a DFT-based average-atom Purgatorio model, which agrees well with PIMC, but is slightly stiffer. Overall, we demonstrate that PIMC is an important tool to benchmark the EOS in the WDM regime. Kohn-Sham based DFT simulations are too inefficient to access physics at temperatures corresponding to the core ionization, and more efficient, but approximate models do not necessarily capture all of the complex physics of the WDM regime.

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