The Kelvin-Helmholtz instability (KHI) is thought to be an important driver for mass, momentum, and energy transfer between the solar wind and magnetosphere. This can occur through global-scale “viscous-like” interactions, as well as through local kinetic processes such as magnetic reconnection and turbulence. An important aspect of these kinetic processes for the dynamics of particles is the electric field parallel to the background magnetic field. Parallel electric field structures that can occur in the KHI include the reconnection electric field of high guide field reconnection, large amplitude ion acoustic waves, as well as time domain structures (TDS) such as double layers and electrostatic solitary waves. In this study, we present a survey of parallel electric field structures observed during three Kelvin Helmholtz events observed by NASA’s Magnetospheric Multiscale (MMS), each at different positions along the magnetosphere’s dusk flank. Using data from MMS’s on-board solitary wave detector (SWD) algorithm, we statistically investigate the occurrence of TDS within the KHI events. We find that early in the KHI development, TDS typically occur in regions with strong field-aligned currents (FACs) on the magnetospheric side of the vortices. Further down the flanks, as the vortices become more rolled up, the prevalence of large electric currents decreases, as well as the prevalence of SWDs. These results suggest that as the instability develops and vortices grow in size along the flanks, kinetic-scale activity becomes less prevalent.

Keywords: Kelvin–Helmholtz instability, flank magnetopause, electrostatic solitary waves, satellite observation, magnetospheric multiscale (MMS)
INTRODUCTION

In addition to magnetic reconnection at the dayside magnetopause, viscous-like interactions at magnetospheric flanks are also thought to transfer energy and momentum from the solar wind to the magnetosphere (Axford and Hines, 1961). This viscous-like interaction is also important for the transfer of energy and momentum from the solar wind to the magnetospheres of gas giants, such as Jupiter and Saturn (Johnson et al., 2014). Although it was once unclear what these “viscous” interactions were, the main mechanism by which this momentum and energy transfer occurs along the magnetospheric flanks is now thought to be the Kelvin-Helmholtz instability (KHI) (Hasegawa et al., 2004; Johnson et al., 2014; Kavosi and Raeder, 2015). The KHI manifests as surface waves that form on the magnetopause in response to flow shear between the magnetosheath and magnetospheric plasma. In the non-linear phase of the instability, these surface waves roll up and form vortices that propagate anti-sunward down the flanks (Johnson et al., 2014).

The mechanisms by which the KHI transfers energy and momentum from the solar wind to the magnetosphere is a topic of ongoing study. One mechanism that has been suggested to facilitate this transfer is magnetic reconnection as the KHI grows, converging flows on the edges of the vortices lead to compressed current sheets where magnetic reconnection can occur, facilitating the mixing and transport of plasma across the magnetopause boundary (Nakamura et al., 2013). Additionally, reconnection can occur on current sheets within the vortices (Nykryi and Otto, 2001) and at higher latitudes as the instability twists up the magnetic field (Johnson et al., 2014). Further, in the intervals between the compressed current sheets, simulations show that turbulence can develop within the vortices as they roll up (Karimabadi et al., 2013; Nakamura and Daughton, 2014). Turbulent cascades transfer energy from large to small scales and can lead to a variety of kinetic processes that dissipate the injected energy and can heat particles in the plasma. Additionally, reconnection could occur on intermittent current sheets that develop in a turbulent cascade (Phan et al., 2018; Sharma-Pyakurel et al., 2019).

On September 8, 2015, the NASA Magnetospheric Multiscale mission, which was launched to study the physics of collisionless magnetic reconnection, observed a KHI event in the post-noon sector of the flank magnetopause for a prolonged (∼3 h) period during northward interplanetary magnetic field (IMF) conditions. The presence of periodic compressed current sheets in the equatorial plane were confirmed, with reconnection jets observed in ∼50% of the current sheets (Eriksson et al., 2016a). Additionally, between the compressed current sheets, the spectra of the magnetic field fluctuations showed a power law indicative of fully developed turbulence, as well as the presence of intermittent currents at small scales (Stawarz et al., 2016). There was also evidence for the mixing of multiple particle populations in the middle of the vortices, leading to strong ion-acoustic-like parallel electric field fluctuations that did not appear to be current-driven (Wilder et al., 2016a; Wilder et al., 2020). The study of another KHI event, on September 27, 2016, suggested that lower hybrid waves that arise during the instability could also facilitate the diffusion of plasma across the flank magnetopause (Tang et al., 2018).

One aspect of the KHI that has not been observed in detail is the role of non-linear plasma structures in dissipating the turbulence. In particular, we focus on broadband electric field solitary structures called “Time Domain Structures” (TDS) (Mozer et al., 2015). These structures are typically on the order of a few to 10’s Debye lengths, and move at speeds ranging from the ion acoustic to the electron thermal speed. Due to their small size, they manifest as short time-duration fluctuations in the electric field, typically in the component of the electric field parallel to the background magnetic field $E_{\parallel}$. These structures include unipolar parallel electric field structures with a net electrostatic potential, such as double layers, as well as bipolar electric field signatures. These bipolar signatures are often referred to as “electrostatic solitary waves” (ESWs), and can refer to several plasma structures such as electron and ion phase space holes (Muschielli et al., 1999; Main et al., 2006), negative potential electron bunching as a result of non-linear whistler waves (Wilder et al., 2016b) and a variety of structures that arise from the mixing of plasmas with differing temperatures (Holmes et al., 2019). One important aspect of TDS, and particularly the readily observable ESWs, is that they are a sign that there is enhanced kinetic activity in plasma. Oftentimes, ESWs are a result of the non-linear evolution of kinetic instabilities, such as the Buneman and two-stream instabilities (Mozer et al., 2015). For example, streaming instabilities on the separatrix in magnetic reconnection can lead to the presence of ESWs (Graham et al., 2016; Wilder et al., 2017). ESWs can also be the sign of nearby double-layers, as the accelerated electrons on one side of the potential drop can become Buneman unstable (Newman et al., 2001). Therefore, because ESWs are self-sustaining beyond the instability that produces them (Muschielli et al., 2000), the presence of ESWs can be viewed as a “smoking gun” for the presence of kinetic instabilities, as well as their drivers, such as plasma beams. Investigating where TDS are most likely to occur within the larger structure of the KHI can therefore provide information on where the "hot spots" are for kinetic activity within the instability. Further, investigating the prevalence of TDS at different stages of the instability can provide information on how the sub-vortex-scale kinetic activity evolves over time.

The NASA MMS mission’s on-board digital signal processing (DSP) board includes an algorithm to detect TDS, particularly ESWs (Ergun et al., 2016). This solitary wave detector (SWD) algorithm has been tested on THEMIS electric field burst data and detected 70% of ESWs identified by visual inspection, and had a less than 10% “false positive” rate. Analysis of an event in the Earth’s magnetotail observed by MMS suggested comparable success rates for detecting ESWs (Hansel et al., 2021). The SWD algorithm reports a histogram (binned by amplitude) of the total TDS counts detected per reporting period. The reporting period used here is 1s. These data are ideal for studying the occurrence and prevalence of TDS in the KHI, where often, more than an hour of burst observations are available from the MMS spacecraft.
In this study, we investigate three KHI events observed by MMS at different positions along the flanks, and different stages of the instability’s development. We use SWD data to investigate the occurrence and prevalence of TDS both within the vortices for each event, as well as cross-event comparisons. We find that TDS are more likely to occur on the magnetospheric side of the vortex intervals between compressed current sheets, particularly in the presence of turbulent magnetic field fluctuations and enhanced field-aligned currents. We also find that at positions of increasing anti-sunward distances along the flanks, the electric currents within the KHI become weaker, and TDS observed by the SWD become less prevalent.

The study of TDS in the KHI will begin with the September 8, 2015 event. This was the first KHI interval observed by MMS with enough periods to do statistical analysis of the instability. Previous studies of this event have shown magnetic reconnection on compressed current sheets (Eriksson et al., 2016a; Eriksson et al., 2016b), turbulence in the vortex-like intervals between the current sheets (Stawarz et al., 2016), and large-amplitude ion-acoustic waves in the plasma mixing regions on the magnetospheric side of the vortex-like intervals (Wilder et al., 2016a; Wilder et al., 2020).

**THE 8 SEPTEMBER 2015 KELVIN-HELMHOLTZ EVENT**

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–250 km/s (anti-sunward), consistent with magnetosheath plasma. Finally, Figure 1F shows the magnetic field vector, \( \mathbf{B} \), in GSE coordinates. The positive \( \mathbf{B}_y \) component at the end of the interval indicates that the interplanetary magnetic field (IMF) had a northward orientation during this event.

During the slow boundary layer crossing between the magnetosphere and magnetosheath, Figure 1 shows that the spacecraft periodically crossed back and forth between magnetosphere-like and magnetosheath-like plasma. This is most easily seen in the ion spectra (Figure 1A) and ion temperature (Figure 1C). This periodic motion becomes especially pronounced after about 10 UT. During this time, there are also periodic reversals in the \( \mathbf{B}_y \) component, which are signatures of the compressed current sheets predicted by (Nakamura et al., 2013). Eriksson et al. (2016a) showed that approximately 50% of these reversals observed by MMS exhibited signatures of reconnection ion jets. From the top of Figure 1, there was an interval of continuous high rate burst data from MMS between 10:07 and 11:27 UT.

To show the structure of the KHI in more detail, Figure 2 shows a time series of burst data from MMS for three periods of the KHI from the September 8, 2015 event shown in Figure 1. From Figures 2A–B, there are three sudden transitions from hotter magnetosphere-like to cooler magnetosheath-like electrons and ions. Coincident with these transitions is a change in density from small (\( \sim 2-3 \text{ cm}^{-3} \)) to larger (\( \sim 20-30 \text{ cm}^{-3} \)) plasma densities, and a sudden change from higher to lower temperature in both the ions and electrons. Coinciding with each of these three temperature drops, there is a sharp reversal in \( \mathbf{B}_y \) from positive-to-negative, which are signatures of the compressed current sheets predicted by (Nakamura et al., 2013). On the third reversal, there is a significant increase in the ion bulk velocity \( V_y \), seen in Figure 2E. This is one of the reconnection jet intervals reported by (Eriksson et al., 2016a). Figure 2G shows the root-mean-square (RMS) amplitude of \( \mathbf{B}_y \), labeled \( \delta \mathbf{B}_y \). \( \delta \mathbf{B}_y \) was calculated with a window-length of 1 s, and a shift-length of 0.5 s. From Figure 2G, it is apparent that the largest values of \( \delta \mathbf{B}_y \) (>15 nT) occur on the compressed current sheets, with high variability between the current sheets.

Figure 2H shows the electric current density \( \mathbf{J} = ne(\mathbf{V}_i - \mathbf{V}_e) \), where \( n \) is the plasma number density, \( e \) is the electron charge, \( V_i \) and \( V_e \) are the ion and electron bulk velocities, respectively. The current is given in magnetic field-aligned coordinates with \( \mathbf{J}_1 \) being along the background magnetic field as defined by the survey magnetic field data, \( \mathbf{J}_2 \) is along a unit vector in the plane of the MMS spacecraft that is perpendicular to the background magnetic field, and \( \mathbf{J}_3 \) completes the right-handed coordinate system. At each of the compressed current sheets, there is a negative \( \mathbf{J}_1 \), which will be important when determining where in the KHI TDS are most likely to occur.

Between the compressed current sheets, there is a slow rotation of \( \mathbf{B}_y \) from negative back to positive. From Figures 2A–B, magnetosphere-like plasma begins to appear during this rotation. Additionally, there is high variability in \( \delta \mathbf{B}_y \), though it does not quite reach the large values seen coincident with the compressed current sheets. This region is where the “vortex”-like structures in the KHI between the compressed current sheets exist, and has been shown to exhibit turbulent cascades and magnetic field intermittency (Stawarz et al., 2016), as well as the presence of large-amplitude ion acoustic waves where the magnetosphere- and magnetosheath-like plasma populations mix (Wild et al., 2016a; Wilder et al., 2020).

Figure 2I shows counts from the lowest amplitude bin (0.5–3 mV/m) from the on-board solitary wave detector (SWD) that is designed to detect ESWs in the burst data (up to 256 kSp/s). The SWD uses one pair of the spin-plane probes and a sliding window of 1/256th of a second, examining the time series electric field data in each window for spikes at least 4x above the pseudo-RMS (Ergun et al., 2016). The number of spike detections are summed over 1s intervals. A version of this algorithm has been checked against THEMIS data and found to detect about 70% of ESWs with a less than 10% false positive rate (Andersson et al., 2009). These spikes are sorted into four amplitude bins: 0.5–3, 3–12, 12–50, and 50 + mV/m, with an instrument saturation at 500 mV/m. In the September 8, 2015 event, the lowest amplitude bin had almost all of the counts, but this is likely due to the fact that the magnetic field has a large Z-GSE component, and therefore, only a small portion of the
parallel electric field will map to a single spin-plane probe pair that is mostly aligned with the X-Y GSE plane. Therefore, the present study will focus on counts from the SWD algorithm rather than the individual amplitude bins. Throughout the interval there is significant variability in the detection of solitary waves, with many of the largest-count intervals occurring in the “vortex” intervals between the compressed current sheet.

As an example of what the SWD detects, Figure 3 shows MMS burst data surrounding the interval with the largest number of counts (>60). From Figure 3A, it can be seen that during the interval with high counts, the electric current density is dominated by $J_l$. The electric field power spectral density, measured by the electric field double probe (EDP) instrument (Lindqvist et al., 2016; Ergun et al., 2016) shows broadband enhancements during this interval as well. No comparable enhancement was seen in the magnetic field spectra (not shown), suggesting that the broadband signals are electrostatic. Figure 3C shows the electric field parallel to the background magnetic field, $E_l$, at 8,192 Samples/s, along with uncertainty in the DC electric field. We see that throughout the interval, the DC $E_l$ is flat, but when the SWD reports enhanced counts, there is significant high frequency activity, as well as spikes. Figure 3E zooms in on the waveform shown in Figure 3C. From left to right, enhanced wave activity is followed by a large bipolar spike, and then a train of shorter duration bipolar spikes. These bipolar spikes are among the types of TDS that the SWD algorithm looks for, and from visual inspection, there are at least 40 ESWs present in the figure, and at least 100 in the entire 1s interval. It is worth noting that the amplitude of the ESWs are larger than the 2.5 mV/
maximum of the SWD bin 1, because the magnetic field is dominated by the Z-GSE component, which is roughly normal to the spin plane of the spacecraft. This was consistently observed for events with high SWD counts throughout the September 8, 2015 event.

**Solitary Wave Detector Statistics**

From Figure 2, it is apparent that the SWD detects TDS throughout the three periods of the KHI, with a high variability in count levels. Additionally, the presence of turbulent cascades in the vortex intervals suggests that the behavior of the instability is highly stochastic, therefore, statistical analysis of SWD detections is needed to determine their occurrence with respect to the larger structure of the KHI. To do this, we calculated 1s averages of plasma data which provides information about the position within the KHI to match the cadence of the SWD. All data comes from the burst interval between 10:07 and 11:27 UT in order to ensure that the time cadence of FPI can be reliably interpolated to the SWD cadence. This is also the interval where the compressed current sheets were observed by (Eriksson et al., 2016a). Histograms of these data are shown by the blue lines in Figure 4. These data in Figure 4 include 1) the magnetic field $B_Y$ (GSE component), 2) the total ion temperature, $T_{ion} = 2T_{ipar} + T_{iperp}$, 3) the ion number density, $N_i$, 4) $\delta B_Y (RMS)$, 5) the ratio of the field-aligned current to total current [$J_{fl}/J_f$], and 6) $J_f$. To determine where TDS were most likely to occur within the instability, 1s events where the SWD counts exceeded 50 were identified. The number 50 was chosen both to ensure there were enough statistics, and also that the 1s intervals would contain significant activity such as shown in Figure 3, rather than just stray solitary waves from spatially or temporally distant kinetic instabilities. For example, if we show statistics of events where the counts exceeded 10, we would have 10,631 intervals out of 18,703, which is more than half of the intervals. Conversely, using a threshold of 50, we were more likely to capture events with large trains of ESWs, like those shown in Figure 3, and the events were rarer, with only 302 intervals of 18,703, or 1.6% of intervals. Histograms of the previously-identified plasma parameters during these events with enhanced SWD counts are shown in red in Figure 4, allowing for comparisons with the “background” distribution of these parameters.

The magnetic field $B_Y$ is helpful in determining where in a given period of the KHI we are likely to see the most ESW activity. From Figure 4A, it is clear that for the high SWD count intervals, the $B_Y$ skews more positive with a mean of 2.7 nT, while for the overall KHI event, $B_Y$ skews negative with a mean of −0.8 nT. This suggests that SWD activity is likely to happen on the “magnetosphere-like” side of the vortices, where the $B_Y$ component is positive. This can also be seen in Figure 4B, where the largest peak in the distribution for high SWD count intervals is when $T_{ion}$ is around 1900 eV. The mean $T_{ion}$ for high SWD count intervals is 1701 eV, while for the overall KHI event it is 1,259 eV, suggesting TDS are more likely to be observed when there is the presence of hotter magnetosphere-like plasma. A similar picture is shown in Figure 4C for $N_i$, with the mean being 9 cm$^{-3}$ for high SWD count intervals, and 12.8 cm$^{-3}$ for the overall event. All of this suggests that while TDS are seen throughout the KHI, there is a bias towards the portion of each period where magnetosphere-like plasma is present. This is consistent with observations of the reconnecting dayside magnetopause, where the bulk of the plasma wave activity occurred on the magnetospheric side of the current sheet (Wilder et al., 2019). It is also similar to the Ion Acoustic Waves (IAWs) observed in the KHI by (Wilder et al., 2020), which seemed to occur on the magnetospheric side of the “vortex” intervals, though in that case, the waves occurred closer to $B_Y = 0$, in a region referred to as the “turbulent mixing region.”

In addition to identifying the presence of compressed current sheets, $\delta B_Y (RMS)$ also provides a measure of how strong the turbulent fluctuations in $B$ are. From Figure 4D, the distribution of $\delta B_Y (RMS)$ for high SWD count intervals largely follows the distribution for the overall event, however, between $\delta B_Y (RMS)$ values of 5 and 15 nT, higher SWD counts are present. This suggests that TDS are more likely to be observed in the presence of turbulent fluctuations. This is different from the IAWs in the KHI, which, while also appearing to occur on the magnetospheric side of the “vortex” intervals, did not appear to be correlated with large $\delta B_Y (RMS)$ (Wilder et al., 2020). These observations of TDS occurring in more turbulent intervals is consistent with Figure 4E, where the histogram for intervals with high SWD counts is skewed towards larger $|J_{fl}/J_f|$ than the overall event, confirming the hypothesis that TDS are more likely to be observed in the presence of enhanced field-aligned currents. It is worth noting that intervals where $|J_{fl}/J_f| > 0.2$ do not have a bias towards the magnetospheric side of the vortices the way the large SWD counts do. For intervals where $|J_{fl}/J_f| > 0.2$, the mean $B_Y$ is ~0.78 nT, while the mean $B_Y$ for the entire event was ~0.76 nT. Surprisingly, there is a bias towards positive $J_f$ for high SWD intervals apparent in Figure 4F. Since the compressed currents are typically intervals with negative $J_f$, this suggests that the most significant ESW activity occurs in the turbulent region. Putting all of this together, the histograms in Figure 4 suggest that the region of largest ESW activity is on the magnetospheric side of the turbulent interval between the compressed current sheets.

**KELVIN-HELMHOLTZ EVENTS FURTHER DOWN THE FLANKS**

The KHI event on September 8, 2015 was observed in the postnoon sector, and therefore was likely early in the development of the KHI. In order to understand how the prevalence and location of TDS evolve as the instability evolves, the analysis in Solitary Wave Detector Statistics is repeated for events further down the Earth’s magnetospheric flank. We introduce two additional KHI events: one on September 27, 2016 and one on September 26, 2017. Figure 5 shows MMS survey data for the two additional events, given in the same format as Figure 1. The September 27, 2016 event was first reported by (Tang et al., 2018). The interval from 19:50–20:06 UT, while shorter in duration than the September 8, 2015 observations, shows similar activity. Specifically, there are periodic boundary crossings apparent in the ion and electron spectra and temperature. There were also...
periodic reversals in the magnetic field GSE $B_Y$ component. One significant difference between the September 27, 2016 event and the September 8, 2015 event was that the periodic fluctuations in the anti-sunward (-$V_X$) component of the flow were much larger compared to the maximum negative value than in the September 8, 2015, suggesting more “rolled up” conditions. This will be investigated further in Event Comparison.

The September 26, 2017 event has, to our knowledge, not been previously reported. From Figure 5, there are some immediate similarities with the other events. First, between 16:50 and 19:00 UT, there were periodic boundary crossings apparent in the ion and electron spectra and temperature, as well as the plasma density, with a dominant periodicity of 230°s, which is longer than the terminator event (~45°s) (Tang et al., 2018) One difference is that the reductions in the anti-sunward flow are even more significant than in the other two events. The challenge in analyzing this event is that immediately after this event is that immediately after the plotted interval in Figure 5, the MMS exited fast survey mode, and therefore the complete crossing into the magnetospheric side of the boundary was not recorded. This makes linear growth analysis difficult; however, given the similarities with the other events, as well as behavior consistent with rolled up vortices (Event Comparison), the interval is likely a KHI event.

Figure 6 shows the locations of the MMS constellation in the X-Y GSE plane when it observed the three events, with the dashed line being the nominal magnetopause as determined by (Shue et al., 1997). From Figure 6 it is clear that the magnetosphere was more compressed than usual, since all three spacecraft observed the magnetopause inside the nominal location. Additionally, the three events exist on three different positions along the flanks. The September 8, 2015 event previously discussed is in the post-noon sector but still on the dayside and will be referred to as the “post-noon” event henceforth. The September 27, 2016 event was near the dusk terminator (X ~ 0 Re) and will be referred to as the “terminator” event. Finally, the September 26, 2017 event was approximately ~9 Re down the dusk flank and will be referred to as the “down-tail” event. For the terminator and down-tail events, the MMS burst data coverage is less frequent than in the post-noon event; however, the burst selections that were downlinked still managed to capture 16 and 25 periods for the terminator and down-tail events, respectively.

Figure 7 shows solar wind conditions for each event from the OMNI database (King and Papitashvili, 2005). All three events exhibit northward IMF $B_Z$ conditions, although the downtail exhibits a brief southward turning of the IMF. The relative strength of $B_X$, $B_Y$, and $B_Z$ also varies between events, with the September 8, 2015 being the most IMF $B_Z$-dominant. The solar wind was fastest during the post-noon event, and slowest during
the downtail event. Because each event is occurring during a different year and under different solar wind conditions, it is impossible to do a one-to-one comparison, however, it is worth comparing events at different positions and under different IMF conditions to determine how the behavior of TDS in the KHI varies. One thing that can be quantified is the state of vortex rollup for each event, which is discussed in Event Comparison.

**Event Comparison**

From Figure 5, there are some similarities between the post-noon event and the two events further down the flank. In all three, there are periodic crossings of the boundary as seen in the spectra, temperature and density plots. Additionally, both events show frequent reversals of the $B_y$ component. One striking difference is that for the terminator and down-tail events, there are larger oscillations in $V_X$, suggesting that the instabilities were at a later stage in the development of the KHI. To test this, the method for identifying rolled up vortices given by (Hasegawa et al., 2004) was used. To do this, the velocity along the flow shear direction, $V_M$, vs. ion number density, $N_i$, is plotted, shown in Figure 8 for all three events. Coordinates were chosen so that $V_M$ is approximately sunward along the flanks. From Figure 8A, which shows data from the post-noon event, there is an approximately linear relationship between the velocity and density, with the lower density (magnetosphere-like) plasma being roughly stationary and the higher density (magnetosheath-like) plasma flowing anti-sunward. This is consistent with the early stages of the instability where the vortices have not fully rolled up (Hasegawa et al., 2004). From Figure 8B, which shows data from the terminator event, there is an increasingly non-linear relationship between velocity and density, with more of the lower density population moving anti-sunward along with the high-density population. The rolled-up state for the terminator event has already been reported by (Tang et al., 2018). The data from the down-tail event, shown in Figure 8C, shows an even more nonlinear relation, with a significant portion of the lowest density plasma moving at the same anti-sunward speed as the high-density population. This suggests an increasing state of roll-up for the instability as it is observed at different positions down the flanks, with the post-noon event not having rolled up vortices, and the down-tail exhibiting the most non-linear “rollup” (Hasegawa et al., 2004).

Since the three events at different positions along the flanks exhibit different amounts of “rollup” in the vortices, they can be used to study the occurrence and prevalence of TDS at different stages of the instability. Figure 9 shows histograms of SWD bin 1 counts for all three events. The time interval used for the post-noon event was the 10:07–11:27 UT burst interval studied by (Eriksson et al., 2016a). For the terminator event, the time period from 19:50–20:06 UT was used, which was the most similar in behavior to the post-noon event. For the down tail event, times from 16:50–19:00 UT were used, which was when periodic boundary crossings comparable to the other two events were observed. From Figure 5, contiguous burst data was not available, and so only times when burst selections were made were used. Comparing Figures 9A,B, the post-noon and terminator events show comparable prevalence of SWDs. One difference with the terminator event is that there are significantly more counts found in bin 2 (not shown) than in the post-noon event. This suggests that there was more ESW activity in the terminator event, which could point to the presence of more kinetic instabilities in the non-linear stage in this event. This can also be seen in the number of 1s intervals where the SWD counts exceeded 50, which were 358 out of 3,280, or ∼11% of intervals. For the down-tail event, shown in Figure 9C, the SWD counts were much lower. There were no intervals where the counts exceeded 50. Using a much smaller threshold of 10 counts, we found 41 out of the 11,200 1s intervals, or 0.3%. This suggests that TDS activity was extremely rare during the event.
FIGURE 8 | $V_{i}\theta$ vs. plasma number density color coded by ion temperature, for three K-Helmholtz intervals on (A) 2015-09-08, (B) 2016-09-27, and (C) 2017-09-26.

FIGURE 9 | Histograms of SWD bin 1 counts for the three KHI intervals on (A) 2015-09-08, (B) 2016-09-27, and (C) 2017-09-26.
Figure 10 shows histograms of the magnitude of electric current density measured by FPI for all three events using the same time ranges as Figure 9. From Figure 10, the post-noon event exhibits the strongest currents and the electric current density on average becomes weaker for observations at increasing anti-sunward distances along the flank. Since from Figures 4E,F, high SWD counts tend to occur in the presence of large field-aligned current, one expects the SWD counts to be lower for the down-tail event, and this could be one explanation of the low prevalence of solitary waves shown in Figure 8C. One possible explanation for this is that as one moves further down the flanks, the vortices may grow in size. Additionally, the magnetic field on the magnetospheric side becomes weaker. These two conspire to reduce $\nabla \times B$, and therefore the current.

**Solitary Wave Detector Statistics**

In order to compare the occurrence of solitary waves in the terminator and down-tail event with the post-noon event, the analysis from *Solitary Wave Detector Statistics* is repeated for each event. Figure 11 shows histograms of plasma parameters during the post-noon event, given in the same format as Figure 4, using the burst interval from 19:50 to 20:06 UT. This burst interval was chosen because it was when the periodicity was most apparent, as well as the presence of reversals in the $B_Y$. This allows for more ready comparison to the September 8, 2015 event. From Figure 11, several similarities between the post-noon event and the terminator event are apparent. First, from Figure 11A, there is still a bias in the high SWD count events towards positive $B_Y$ in comparison to the histograms for the overall event. This bias is not as apparent as in the post-noon event, however. Additionally, high SWD count intervals are still more likely to occur in the presence of field-aligned currents, although the bias towards positive currents is no longer as strong. Further, the high SWD count histograms are more spread in temperature and density in the terminator event than in the post-noon event, suggesting SWDs are more evenly distributed throughout the interval. One reason for this may be the increase “rolled up” state of the vortices in the terminator event versus the post-noon event, leading to the plasma being more mixed.

Figure 12 shows histograms for the down-tail event given in the same format as Figures 4, 11, using all burst data between 16:50 to 18:20 UT. For Figure 12, the threshold for “high SWD counts” for bin 1 was reduced to 10, given the reduced prevalence in solitary wave activity shown in Figure 9. Several similarities and several differences are immediately apparent. First, for the overall event, the temperatures were significantly lower and the $B_Y$ was most likely negative, suggesting most of the observations during this event occurred on the magnetosheath side of the vortices. This may be a possible explanation for the reduced SWD counts shown in Figure 9 for the down-tail event, since in the post-noon and terminator events, higher SWD count events were more likely to be seen on the magnetospheric side. However, in the post-noon and terminator event, there were still high SWD count events even on the magnetosheath side. Therefore, the event seems to simply just have less activity that would lead to the presence of TDS. One similarity between all three events is seen in Figure 12E, where the high SWD count intervals are biased towards intervals with enhanced field-aligned currents.
SUMMARY AND CONCLUSION

In this study, we investigated the occurrence and prevalence of time domain structures (TDS) in the Kelvin-Helmholtz instability (KHI) observed by MMS at different positions along the dusk magnetospheric flank. The events investigated included an event observed in the post-noon sector on September 8, 2015, one near the dusk terminator on September 27, 2016 and one further down the magnetospheric flanks on September 26, 2017. In each event, a different stage of the instability’s development were observed, with the post-noon event including the least rolled up vortices, and the down-tail event having the most. To investigate the location of TDS in the vortices for each event, we used data from the MMS mission’s on-board solitary wave detector (SWD) algorithm (Ergun et al., 2016). For each event, we identified 1s intervals where the SWD counts exceeded a threshold, and then investigated the plasma parameters where these intervals were most likely to occur.

In the post-noon event, it was shown that intervals with high SWD counts were more likely to be on the magnetospheric side of the “vortex” intervals between the compressed current sheets. This was similar to the observations of ion-acoustic waves during the post-noon event, which found the waves were most likely to occur on the magnetospheric side (Wilder et al., 2020). One difference between the prevalence of TDS and ion-acoustic waves is that the latter did not appear to have any correlation with the

![Figure 11](https://example.com/figure11.png)

**FIGURE 11** | Histograms of magnetic field and plasma quantities during the September 27, 2016 burst interval, given in the same format as Figure 4. (A) Magnetic field GSE $B_y$, (B) Ion temperature, $T_{ion}$, (C) Ion number density, $N_i$, (D) $\delta B_y$ RMS, (E) $|J_i|$, (F) $J_i$.
presence of magnetic fluctuations, while in the present study, intervals with high SWD counts were more likely to be seen when moderate-to-large (10–20 nT) RMS fluctuations in the magnetic field normal to the magnetopause boundary. It was also shown that high SWD count intervals were more likely to be observed during times when the field-aligned current was significant compared to the total current density. This is consistent with the idea that the instabilities and processes that can drive TDS (e.g., double layers, streaming instabilities) are likely to occur in the presence of strong FACs (Ergun et al., 2001; Mozer et al., 2014). One surprising result was that the intervals with high SWD counts were more likely to occur on positive field-aligned currents, while the compressed current sheets are negative. This suggests that the processes that drive TDS in the KHI are more likely to occur inside the vortices rather than on the compress current sheets on the edge. Also—since the TDS seem to occur in the presence of currents, while the previously-reported ion-acoustic waves do not, the present study supports the hypothesis by (Wilder et al., 2016a, Wilder et al., 2020) that the ion-acoustic waves in the KHI are driven by plasma mixing rather than being current-driven.

One immediate difference between the three events was that the down-tail event had significantly less SWD counts than the post-noon and terminator. Consistent with this, MMS also observed increasingly weak electric current densities as the KHI evolved towards more rolled up vortices. It is unclear why this happens, but one hypothesis is that as the KHI evolves along the flank, the smaller-scale turbulent features

FIGURE 12 | Histograms of magnetic field and plasma quantities during the September 26, 2017 burst interval, given in the same format as Figure 4. (A) Magnetic field GSE $B_y$, (B) Ion temperature, $T_{ion}$, (C) Ion number density, $N_i$, (D) $\delta B_Y,\text{RMS}$, (E) $|J_\parallel/|J|$, (F) $J_\parallel$.  

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largely dissipate by the time the vortices reach an anti-sunward distance of ~10 Re from the terminator. Another hypothesis is that the vortices may grow in size as they propagate down the flanks, and since the magnetic field also becomes weaker at increasing distance from Earth, the electric current densities become smaller by way of Ampère's law. This is consistent with the reduced SWD counts in the down-tail event, as for all three events, the intervals with higher SWD counts were more likely to occur in the presence of field-aligned currents. More events along the flanks need to be studied to understand the difference in electric current density between observations of the KHI at different positions along the flanks.

The importance of the KHI for magnetospheric physics is that it is thought to be one of the mechanisms by which energy and momentum are transferred from the solar wind to the magnetosphere Axford and Hines, 1961; Kavosi and Raeder, 2015. Exactly how this transfer is facilitated is a topic of ongoing research. Suggested mechanisms include magnetic reconnection (Nykjyr and Otto, 2001; Nakamura et al., 2013, Eriksson et al., 2016a) and diffusion via particles interacting with waves, such as lower hybrid waves (Tang et al., 2018). Turbulent cascades have also been observed within the vortices (Stawarz et al., 2016), and it is unclear how they impact the overall mass-energy transfer in the KHI. It has long been suggested that time domain structures and parallel electric fields may be a mechanism by which turbulent cascades can be dissipated. For example, electron phase space holes and double layers have been observed in the bursty bulk flow braking region, where magnetic field spectra consistent with a turbulent cascade were observed (Ergun et al., 2014; Stawarz et al., 2015). The present study shows that TDS tend to occur on the magnetospheric side of the vortices near strong fluctuations in the magnetic field and field-aligned currents, which suggests that the processes that lead to their occurrence are also likely to happen there. Future studies should investigate what these processes and instabilities that lead to the presence of TDS are, and what role they play in the overall mass/energy transfer between the solar wind and magnetosphere, as well as the dissipation of turbulence on the flanks.

DATA AVAILABILITY STATEMENT

Publicly available datasets were analyzed in this study. This data can be found here: https://lasp.colorado.edu/mms/sdc/public/.

AUTHOR CONTRIBUTIONS

FW performed the bulk of the analysis and wrote the paper, RE developed the SWD algorithm, DG and SE identified KHI events for study, PH and DM assisted in validating the SWD algorithm, NA calibrated the electric field booms, JB and RT confirmed appropriate use of MMS data and worked as scientist in the loop to identify events, RS calibrated the magnetometer, BG calibrated the fast plasma investigation.

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