MAGNETIC FIELDS AND THE OUTER ROTATION CURVE OF M31

B. Ruiz-Granados1,2, J. A. Rubiño-Martín1,2, E. Florido3,4, and E. Battaner3,4
1 Instituto de Astrofísica de Canarias (IAC), E-38200, La Laguna, Tenerife, Spain
2 Departamento de Astrofísica, Universidad de La Laguna, E-38205, La Laguna, Tenerife, Spain
3 Departamento Física Teórica y del Cosmos, Universidad de Granada, Granada, Spain
4 Instituto de Física Teórica y Computacional Carlos I, Granada, Spain

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ABSTRACT

Recent observations of the rotation curve of M31 show a rise of the outer part that cannot be understood in terms of standard dark matter models or perturbations of the galactic disk by M31’s satellites. Here, we propose an explanation of this dynamical feature based on the influence of the magnetic field within the thin disk. We have considered standard mass models for the luminous mass distribution, a Navarro–Frenk–White model to describe the dark halo, and we have added up the contribution to the rotation curve of a magnetic field in the disk, which is described by an axisymmetric pattern. Our conclusion is that a significant improvement of the fit in the outer part is obtained when magnetic effects are considered. The best-fit solution requires an amplitude of ~4 μG with a weak radial dependence between 10 and 38 kpc.

Key words: galaxies: individual (M31) – galaxies: magnetic fields

1. INTRODUCTION

Recent high sensitivity measurements of the rotation curve of M31 (Chemin et al. 2009; Corbelli et al. 2010, hereafter C09 and C10, respectively) suggest that it highly rises at the outermost part of the disk of M31 ($r \gtrsim 25–30$ kpc, see Figure 1). This behavior cannot be considered an exception. Similar outer rising rotation curves can be found in other galaxies. Noordermeer et al. (2007, p. 1522) stated that “in some cases, such as UGC 2983, UGC 3993, or UGC 11670, there are indications that the rotation curves start to rise again at the outer edges of the H i disks,” suggesting follow-up observations of higher sensitivity to investigate this fact in more detail. Other examples could be found in some rotation curves provided by Spano et al. (2008), in particular the curves of UGC 6537 (SAB(r)c), UGC 7699 (SBcd/LSB), UGC 11707 (Sadm/LSB), or UGC 11914 (SA(r)ab) measured by means of Fabry–Perot spectroscopy. Other potential examples could be NGC 1832 and NGC 2841 (Kassim et al. 2006), even with a larger error, and ESO 576-G51 and ESO 583-G7 (Seigar et al. 2005), even if the outer rising is small. Potential nearby candidates could be NGC 3198, DDO 154, or NGC 7331 (de Blok et al. 2008). Therefore, outer rising rotation curves are not uncommon in spirals, being the case of M31 the most representative. This puzzling dynamic feature requires a theoretical explanation. A detailed study by C09 showed that the Navarro–Frenk–White (NFW), Einasto, or pseudoisothermal dark matter halos fail to reproduce the exact shape of the rotation curve of M31 in the outer region and found no differences between the various halo shapes. Moreover, they found new H i structures as an external arm and thin H i spurs in the outskirts of the disk. These spurs have also been observed by Braun et al. (2009). Thus, a primarily explanation of this gas perturbations could be the interactions with the M31’s satellites as NGC 205 (Geehan et al. 2006; Corbelli et al. 2010). The main problem of matching the properties of the giant stellar stream observed in the south of M31 (Ibata et al. 2001) is that the orbital of the companion that produce the stream is not constrained satisfactorily (Fardal et al. 2006), or high velocities for the radial orbits are found (see, e.g., Howley et al. 2008). Although the northeastern (NE) and southwestern (SW) parts of M31 show different kinematical properties, both suggest a rise in the outer part of the rotation curve (see Figures 5 and 6 in C09 and C10, respectively).

In this work, we show that magnetic dynamic effects constitute a clear and simple basis to interpret this feature. Some particular models of magnetically driven rotation curves have been presented (Nelson 1988; Battaner et al. 1992; Battaner & Florido 1995, 2000, 2007; Kutschera & Jalocha 2004; Tsiklauri 2008). Although those models were originally developed to explain flat rotation curves without dark matter, our purpose here is more conventional and we will consider the contribution of both an NFW dark matter halo and a magnetic field added to match the velocity in the outermost region.

Magnetic fields are known to slowly decrease with radius (see, e.g., Beck et al. 1996; Han et al. 1998; Beck 2001, 2004, 2005), and therefore they become increasingly important at the rim. For large radii, an asymptotic $1/r$-profile for the field strength provides an asymptotic vanishing magnetic force. This $1/r$-profile has been found to match the polarized synchrotron emission of the Milky Way (Ruiz-Granados et al. 2010) and NGC 6946 (Beck 2007), and will be considered in this work.

2. MASS MODELS AND THE MAGNETIC FIELD OF M31

In this section, we briefly present the luminous and dark mass models used to describe the observational rotation curve of M31. As we are interested in the outer region (i.e., distances higher than 10 kpc), we follow C10 and neglect the bulge contribution. We will also adopt from C09 and C10 the parameters describing stellar disk and gaseous distribution, respectively. Therefore, we will only leave as free parameters those describing two physical components: the dark matter halo and the magnetic field.

2.1. Disk Model

The stellar disk is assumed to be exponential (Freeman 1970), being the surface mass density

$$\Sigma = \Sigma_0 \exp \left( -\frac{r}{R_d} \right),$$

(1)
where $\Sigma_0$ is the central density of stars and $R_d$ is the radial scale factor.

The contribution to the circular velocity of the stellar disk is (see Binney & Tremaine 1987)

$$v_d(R) = 4\pi G \Sigma_0 R_d y^2 [I_0(y)K_0(y) - I_1(y)K_1(y)],$$

where $y = R/2R_d$ and $I_0, K_0, I_1, K_1$ are the modified Bessel’s functions for first and second orders.

The gaseous disk mainly contains H i, molecular gas, and helium. The estimated gaseous distribution of M31 represents approximately a 9% (for C09) and 10% (for C10) of the total helium. The estimated gaseous distribution of M31 represents

$$\Sigma = 0.20 \times \rho_c R_d,$$

where $c$ is the concentration parameter of the halo which is defined as $c = R_{200}/R_h$, and $R_{200}$ is the radial scale factor. The contribution to the circular velocity due to this profile is given by Navarro et al. (1997)

$$v_h(R) = V_{200} \sqrt{\frac{1}{x} \ln(1+c x) - \frac{c x}{1+c x}},$$

where $V_{200}$ is the velocity at the virial radius $R_{200}$ which is assumed $\sim 160 \text{ kpc}$ for C09 and $R_{200} \sim 200 \text{ kpc}$ for C10, $c$ is the concentration parameter of the halo which is defined as $c = R_{200}/R_h$, and $x$ is $r/R_{200}$. According to C09 and C10, the total dark halo mass at the respective virial radius is $M_{200} \sim 10^{12} M_\odot$. Our free parameters are $V_{200}$ and $c$. Values from C09 are $c = 20.1 \pm 2.0$ and $V_{200} = 146.2 \pm 3.9 \text{ km s}^{-1}$. Values from C10 are $c = 12$ and $V_{200} \sim 140 \text{ km s}^{-1}$.

### 2.2. Halo Model

The dark matter halo is described here by an NFW profile (Navarro et al. 1996)

$$\rho_h(R) = \frac{\delta_c \rho_c}{r/R_c [1 + (r/R_c)^{2}]^2},$$

where $\delta_c$ is a characteristic density contrast, $\rho_c = 3H_0^2/8\pi G$ is the critical density, and $R_h$ is the radial scale factor. The contribution to the circular velocity due to this profile is given by

$$v_h(R) = V_{200} \sqrt{\frac{1}{x} \ln(1+c x) - \frac{c x}{1+c x}},$$

where $V_{200}$ is the velocity at the virial radius $R_{200}$ which is assumed $\sim 160 \text{ kpc}$ for C09 and $R_{200} \sim 200 \text{ kpc}$ for C10, $c$ is the concentration parameter of the halo which is defined as $c = R_{200}/R_h$, and $x$ is $r/R_{200}$. According to C09 and C10, the total dark halo mass at the respective virial radius is $M_{200} \sim 10^{12} M_\odot$. Our free parameters are $V_{200}$ and $c$. Values from C09 are $c = 20.1 \pm 2.0$ and $V_{200} = 146.2 \pm 3.9 \text{ km s}^{-1}$. Values from C10 are $c = 12$ and $V_{200} \sim 140 \text{ km s}^{-1}$.

### 2.3. The Regular Magnetic Field of M31

The first measurements of the magnetic field of M31 were obtained by Beck (1982) using the polarized synchrotron emission at 2700 MHz, showing that a magnetic pattern was aligned with H i structures and formed a ring at $r \sim 1 \text{ kpc}$ of height above the galactic plane. However, recently, Stepanov et al. (2008) have shown that these results contained a significant contribution of Galactic foregrounds, and so it is difficult to infer the model from these measurements. In any case, as we show below, the detailed structure of the field is not relevant for the rotation curve.

Fletcher et al. (2004) presented a detailed study of the regular field of M31 based on multi-wavelength polarized radio observations in the region between 6 and 14 kpc. By fitting the observed azimuthal distribution of polarization angles, they found that the regular magnetic field follows an axisymmetric pattern in the radial range from 8 to 14 kpc. The pitch angle decreases with the radial distance, being $p \sim -16^\circ$ for distances $r < 8 \text{ kpc}$, and $p \sim -7^\circ$ for $r < 14 \text{ kpc}$. This fact implies that the field becomes more tightly wound with increasing galactocentric distance. They found a total field strength (i.e., regular and turbulent components) of $\approx 5 \mu G$. For the regular field they found that it became slowly lower, reaching at $r \sim 14 \text{ kpc}$ a strength of $\approx 4.6 \mu G$.

In this Letter, our basic assumption is that the regular magnetic field of M31 is described by an axisymmetric model that extends up to 38 kpc. For this model, the components in cylindrical coordinates are given by

$$B_r = B_0(r) \cos(p),$$

$$B_\theta = B_0(r) \sin(p),$$

where $p$ is the pitch angle and $B_0(r)$ is the field strength as a function of the radial distance. As shown below, from the point of view of the description of the rotation curve, the relevant component is $B_\theta$. Here, we will assume that $p = 0^\circ$, as we are mostly interested in the outer region where $p$ is very low. Several previous probes also indicate low values of $p$. In any case, this is not a strong assumption in the sense that a non-zero field value can be absorbed into the field strength ($B_1$) as a different amplitude. For the field strength, as a baseline computation, we shall consider a radial dependence of $B_0(r)$ or equivalently $B_\theta$ given by

$$B_\theta(r) = B_1 \frac{r_1}{r_1 + r},$$

where $r_1$ represents the characteristic scale at which $B_0(r)$ decreases to half its value at the galactic center and $B_1$ is an amplitude in which we are absorbing the $\cos(p)$ factor. This expression has an appropriate asymptotic behavior, in the sense that we obtain a finite value when $r$ is close to the galactic center ($r \to 0$), and asymptotically tends to $\propto 1/r$ when $r \to \infty$, as suggested by Battaner & Florido (2007). Observations carried out by Fletcher et al. (2004) established that

$$B_\theta(r = 14 \text{ kpc}) \approx 4.6 \mu G.$$

This observational value at this radius was considered as fixed in our baseline computation. By substituting into Equation (7), we can find a relation between $B_1$ and $r_1$ that allows us to re-write Equation (7) in terms of a single free parameter ($r_1$)

$$B_\theta(r) = \frac{4.6 r_1 + 64.4}{r_1 + r},$$

where $r$ is given in kpc and $B_\theta(r)$ in $\mu G$.

### 3. METHODOLOGY

#### 3.1. Observational Rotation Curve of M31

We have considered the two data sets from C09 and C10. They consist of a set of 98 and 29 measurements of the circular velocity (and their associated error bars), respectively, which were obtained with the high-resolution observations performed with the Synthesis Telescope and the 26 m antenna at the Dominion Radio Astrophysical Observatory (C09) and with the wide-field and high-resolution H i mosaic survey done with the help of the Westerbork Synthesis Radiotelescope and the
Robert C. Byrd Green Bank Telescope (GBT; Braun et al. 2009). For our purposes, we consider only distances higher than \( r > 10 \) kpc to illustrate the effects of the magnetic field. The actual data points on the rotation curve were obtained after fitting a tilted ring model to the data and assuming a distance to M31 of 785 kpc. C09 derived a value of the inclination angle of \( i \sim 74^\circ \), which is lower than that derived from optical surface photometry measurements (Walterbos & Kennicutt 1987) and by C10 (\( i \sim 77^\circ \)). The data points are plotted in Figure 1 in two separate panels.

3.2. Influence of the Magnetic Field on the Gas Distribution

The presence of a regular magnetic field affects the gas distribution (Battaner et al. 1992; Battaner & Florido 1995, 2000). The fluid motion equation can be written as (see, e.g., Battaner 1996)

\[
\rho \frac{\partial v_0}{\partial t} + \rho v_0 \cdot \nabla v_0 + \nabla P = n \dot{F} + \frac{1}{4 \pi} B \cdot \nabla B - \nabla \left( \frac{B^2}{8 \pi} \right),
\]

where \( \rho \) is the gas density, \( \dot{v_0} \) is the velocity of the fluid, \( P \) is the pressure, \( \dot{F} \) is the total force due to gravity, and \( B \) is the magnetic field. We assume standard MHD conditions, i.e., infinite conductivity. Equation (10) is simplified by assuming axisymmetry and pure rotation, where \( \dot{v_0} = (\dot{v}_r, \dot{v}_\theta, \dot{v}_z) = (0, \theta, 0) \) even if these conditions are not necessary regarding the dynamic effects in the radial direction. Taking into account all these facts, the motion equation in the cylindrical coordinate is

\[
\rho \left( -\frac{d\Phi(r)}{dr} + \frac{\theta^2}{r} \right) - \frac{dP}{dr} - F_{r,\text{mag}} = 0,
\]

where \( \Phi(r) \) is the gravitational potential, \( F_{r,\text{mag}} \) is the radial component of the magnetic force, and \( P \) is the pressure of the fluid. We can assume that pressure gradients in the radial direction are negligible (Battaner & Florido 2000). In this case, then the radial component of the magnetic force is given by

\[
F_{r,\text{mag}} = \frac{1}{4\pi} \left( \frac{B^2}{r} + \frac{1}{2} \frac{dB^2}{dr} \right),
\]

and the contribution of the magnetic field to the circular velocity is given by

\[
v_{\text{mag}} = \frac{r}{4\pi \rho} \left( \frac{B^2}{r} + \frac{1}{2} \frac{dB^2}{dr} \right).
\]

3.3. Modeling the Rotation Curve

The rotation curve is obtained, as usual, by quadratic summation of the different contributions

\[
\dot{\theta}(r)^2 = v_0^2(r)^2 + v_d^2(r)^2 + v_h^2(r)^2 + v_{\text{mag}}^2(r)^2,
\]

where we explicitly set \( v_0(r) = 0 \) as mentioned above.

3.4. Model Selection

For the luminous mass models, the different parameters are considered as fixed values in our analysis (see Table 1). For the NFW dark halo, we constrain the \( V_{200} \) and \( c \) parameters, allowing a range for \( V_{200} \) between 100 and 220 km s\(^{-1}\) with steps of 0.5 km s\(^{-1}\) and \( c \in [5, 30] \) with steps of 0.3 km s\(^{-1}\). The contribution of the magnetic field to the rotation curve is fitted through one free parameter, \( r_1 \), that we are considering which is equivalent to fit \( B_0 \) as we discussed above. For this parameter, we have explored values in the range from 1 to 1000 kpc. Our analysis is based on a reduced-\( \chi^2 \) as the goodness-of-fit statistic. Thus, the best-fit parameters are obtained by minimizing this function

\[
\chi^2 = \frac{1}{N - M} \sum_{i=1}^{n} \frac{(\dot{\theta}_i^{\text{obs}} - \dot{\theta}_i^{\text{model}})^2}{\sigma_i^2},
\]

where \( N \) is the total number of points to which we have measured the rotational velocity and depends on the considered data set (\( N = 74 \) for C09 and \( N = 27 \) for C10), and \( M \) is the number of free parameters. The sum runs over the observational data points, being \( \dot{\theta}_i^{\text{obs}} \) the observed velocity and \( \dot{\theta}_i^{\text{model}} \) the modeled velocity, which depends on the particular model. We shall consider two models: one without magnetic contribution (DM) and another with the magnetic field (DM+MAG). Finally, \( \sigma_i \) is the observational error bar associated with each data point.

4. RESULTS AND DISCUSSION

Our main results are summarized in Figure 1. The dotted line shows our best-fit rotation curve for C09 and C10 when considering only the usual dynamical components (the stellar component and the dark halo at this range of distances), while the solid line shows the result when adding up also the magnetic contribution.

The most important result is that, as shown in Battaner & Florido (2000), the effects of magnetism on the rotation curve are only relevant at large radii (in this case of M31, at distances larger than about 25 kpc). In this sense, the radial range of the data sets of C09 and C10 is optimal to observe the magnetic effects.

Table 2 summarizes our results for the best-fit solutions without (labeled as DM model) and with magnetic field influence (DM + MAG model). As shown, magnetic effects on the gaseous disk significantly decrease the value of the reduced-\( \chi^2 \) statistic for both data sets. Specially for C09, the fit is significantly improved when taking into account a new parameter (\( \Delta \chi^2 = 6.5 \)). The radial scale factor of the magnetic field (\( r_1 \)) is unconstrained in both cases, but shows clear preference for high values, which means that the
best-fit solution for the field slowly decreases with the radial distance in the considered interval (i.e., between 10 and 38 kpc). For example, at \( r \sim 38 \) kpc, the field is found to be \( B_\phi > 4.4 \mu G \) for C09 and \( B_\phi > 4.0 \mu G \) for C10 for this best-fit solution. Both values are compatible with the strength of the field obtained by Fletcher et al. (2004) who found a nearly constant strength of the regular field of about \( \sim 5 \mu G \) between 6 kpc and 14 kpc. Moreover, when no radial variation of the strength is considered (i.e., if \( r_l \to \infty \)) and we fit for the amplitude \( B_\phi \), we obtain that \( B_\phi = 4.7^{+0.7}_{-0.6} \mu G \) which is again compatible with results discussed above. This suggests that the data do not require an important radial variation of the strength of the field for the considered range of distances, or in other words, the contribution of the second term in the right-hand side of Equation (12) is negligible (i.e., \( dB_\phi/dr \ll B_\phi/r \)). Therefore, if we had considered another radial profile (e.g., exponential), we would have found a large radial scale factor too. The azimuthal component of the field is practically constant between 10 and 38 kpc.

Our results imply large magnetic fields at large radii. How these are produced lies beyond our scope. On the other hand, we would expect the extragalactic field to be also of this order of magnitude. Theoretical predictions (Dar & de Rújula 2005) suggest values of the level of few \( \mu G \) for the intergalactic magnetic fields (IGMF). Kronberg (1994), Govoni & Feretti (2004), and Kronberg (2005) have reviewed observations of \( \mu G \) level in rich clusters, though no direct measurements have been reported for the IGMF in the Local Group near M31. The observational evidence for IGMF is still weak, but quite strong IGMF near galaxies cannot be disregarded.

We finally note the apparent discrepancy between our derived parameters for the DM model and those obtained by C09 and C10 (see Section 2.2). However, it is important to stress that we are restricting the fit to the outer region of M31 (\( r > 10 \) kpc). In this outer range, there is a weaker dependence of the shape of the rotation curve on the concentration parameter \( c \), and thus lower values of \( c \) are found because the fit tries to compensate the rising behavior in the outer part. The inclusion of the magnetic field corrects this apparent model obtained without the contribution of the magnetic field.

5. CONCLUSIONS

The rotation curve of M31 (Chemin et al. 2009; Corbelli et al. 2010) is rather representative of the standard rotation curves of spirals for \( r < 30 \) kpc, but it seems to rise out to, at least 38 kpc, the limiting distance of the observations. Indeed, this behavior is not restricted to M31, and we are probably dealing with a common dynamical feature of many other spirals. Therefore, the outermost rising rotation curve is a very important theoretical challenge.

It is certainly a challenge as the standard dark matter halo models, in particular the universal NFW profiles, do not account for this dynamical unexpected behavior.

A conventional galactic model, with bulge, disk, and dark matter halo, has been shown to provide good fit to the data in the range \( r < 20 \) kpc (C09, C10). Here, we take advantage of these results and do not fit any of the luminous components, which are taken to be exactly the same as those proposed by C09 and C10. We have restricted our study to the region \( r > 10 \) kpc, and we only fitted the parameters describing the dark matter halo, and the magnetic field contribution. Our main conclusion is that magnetic fields are not ignorable for explaining large-scale dynamic phenomena in M31, producing a significant improvement of the fit of the rotation curve at large distances. Moreover, the required field strength of the regular component (\( B_\phi \sim 4 \mu G \)) is fully consistent with the measured magnetic field in M31 at least up to \( r \sim 15 \) kpc.

This conclusion seems very reasonable, as magnetic fields are amplified and act “in situ,” and therefore they become increasingly important at the rim, where gravity becomes weaker.

The best-fit model of the magnetic fields requires a field strength slowly decreasing with radius. This slow decrease is compatible with present values of the strength derived from
observations of the polarized synchrotron emission of the disk, but clearly we need measurements of Faraday rotation of extragalactic sources at this large radii to confirm that the magnetic field is present up to this distance and to trace unambiguously the regular component. Hence, future experiments such as LOFAR\(^5\) and SKA\(^6\) (Beck 2009), will be extremely important, allowing a detailed explorations on the galactic edge as well as in the intergalactic medium.

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\(^5\) http://www.lofar.org
\(^6\) http://www.skatelescope.org/