UHECR: Signatures and models

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Abstract. The signatures of Ultra High Energy \((E \gtrsim 1 \text{ EeV})\) proton propagation through CMB radiation are pair-production dip and GZK cutoff. The visible characteristics of these two spectral features are ankle, which is intrinsic part of the dip, beginning of GZK cutoff in the differential spectrum and \(E_{1/2}\) in integral spectrum. Measured by HiRes and Telescope Array (TA) these characteristics agree with theoretical predictions. However, directly measured mass composition remains a puzzle. While HiRes and TA detectors observe the proton-dominated mass composition, the data of Auger detector strongly evidence for nuclei mass composition becoming progressively heavier at energy higher than 4 EeV and reaching Iron at energy about 35 EeV. The models based on the Auger and HiRes/TA data are considered independently and classified using the transition from galactic to extragalactic cosmic rays. The ankle cannot provide this transition, since data of all three detector at energy \((1–3) \text{ EeV}\) agree with pure proton composition (or at least not heavier than Helium). If produced in Galaxy these particles result in too high anisotropy. This argument excludes or strongly disfavours all ankle models with ankle energy \(E_a > 3 \text{ EeV}\). The calculation of elongation curves, \(X_{\text{max}}(E)\), for different ankle models strengthens further this conclusion. Status of other models, the dip, mixed composition and Auger based models are discussed.

1. INTRODUCTION

The observed energy spectrum of Cosmic Rays (CR) has an approximately power-law behavior for 11 orders of magnitude in energy with several features that can be linked with particles propagation and acceleration. This power-law behavior is most probably indicative of a power-law acceleration spectra, while spectral features may be assigned to changes in the origin of particles, their propagation and acceleration.

The most prominent feature is the knee in all-particle spectrum at energy \(3–4 \text{ PeV}\), discovered first at the MSU (Moscow State University) array in 1958 [1]. At the knee the spectrum \(E^{-\gamma}\) steepens from \(\gamma \approx 2.7\) to \(\gamma \approx 3.1\). This knee is provided by the light elements, protons and Helium, and is explained in the framework of the Standard Model (SM) for Galactic Cosmic Rays (GCR) by the maximum energy \(E_{\text{max}}\) of acceleration in the Galactic Sources (Supernovae Remnants, SNRs). In the case of the rigidity-dependent acceleration \(E_{\text{max}} \propto Z\), where \(Z\) is charge number of a nuclei, the maximum acceleration energy is reached by Iron nuclei and the Iron knee is predicted to be located at energy by factor 26 times higher than for proton knee, i.e. at energy \(E_{\text{Fe}}^{\text{max}} \approx 0.1 \text{ EeV}\). Recently, the Iron knee was found indeed at energy 0.8 EeV in KASCADE-Grande experiment [2] in a good agreement with rigidity acceleration prediction.

Above the knee, at energy \(E_{\text{skn}} \approx (0.4–0.7) \text{ EeV}\), there is a faint feature in the spectrum [3] called the second knee. It is seen in many experiments (for a review see [4]). This feature is often interpreted as the place of transition from galactic to extragalactic CRs.

However, for the last forty years the standard place for transition from galactic to extragalactic CRs is considered at ankle, a very prominent spectral feature, observed first in 1960s at Vulcano Ranch detector, and immediately interpreted by J. Linsley [5] as transition between these two components of...
CRs. At present beginning of ankle is determined as $E_{\text{obs}}^{a} \approx 4.6 \text{ EeV}$ according to HiRes observations [6], and $E_{\text{obs}}^{a} \approx (4.0-4.5) \text{ EeV}$ according to Auger (PAO) observations [7, 8].

The highest energy feature, the steepening (‘cutoff’) of the spectrum is found in all three largest detectors, HiRes [9], Telescope Array (TA) [10] and PAO [11], though the nature of this cutoff is still questionable.

The spectral features expected theoretically are much different for UHE protons and nuclei. If primary particles are protons, their spectrum must show a steepening which begins at $E_{\text{GZK}} \sim 50 \text{ EeV}$. This is the famous Greisen [12], Zatsepin and Kuzmin [13] cutoff, referred to as GZK, caused by pion photo-production energy loss in collisions of protons with the CMB photons:

$$p + \gamma_{\text{CMB}} \rightarrow N + \pi.$$  \hspace{1cm} (1)

Most probably this cutoff is already observed in the HiRes [9] and TA [10] data, while the spectrum steepening observed by the PAO [11] does not agree well, according to our calculations, with the predicted GZK shape and position.

There is another feature in the spectrum of UHE extragalactic protons, the pair-production dip, which, as in case of GZK cutoff, can be directly linked to the interaction of CRs with the CMB. This dip arises due to electron-positron production energy loss by extragalactic protons interacting with the CMB photons:

$$p + \gamma_{\text{CMB}} \rightarrow p + e^+ + e^-.$$  \hspace{1cm} (2)

This feature has been studied in [14–18]. The dip was observed with a very good statistical significance, $\chi^2$/d.o.f. $\sim 1$, by the Fly’s Eye, Yakutsk, Akeno-AGASA and HiRes detectors, but it is absent in the Auger (PAO) data (see section 2.4 for a more detailed analysis). A remarkable property of the pair-production dip is an automatic description of the ankle, which appears as a flat intrinsic part of the dip.

The pair-production dip and GZK cutoff are signatures of protons. A confirmation of the shape of these features can be considered as an indirect evidence for a proton-dominated composition of primary CRs. For nuclei as primaries the shapes of the dip and cutoff are much different.

A different explanation of the dip has been proposed by Hill and Schramm [19]. They interpreted the dip observed in 1980s in terms of a two-component model; the low energy component was either galactic or produced by Local Supercluster. A similar model was later considered in [20]. The Hill-Schramm’s interpretation is widely accepted now.

An alternative to the protons as primaries is given by nuclei. Propagating through astrophysical backgrounds, nuclei lose their energy in photo-disintegration and pair production processes, and also due to adiabatic expansion of the universe. The steepening of nuclei spectra due to photo-disintegration in the interactions with the CMB has been shortly mentioned by Greisen [12] and later considered quantitatively in [21–25]. The beginning of the steepening in this case (nuclei in the CMB radiation only) corresponds to the intersection of $e^-e^+$ and adiabatic energy losses curves [22, 23]. The beginning of this steepening is lower than in the case of GZK cutoff and the shape of this feature differs from that of GZK. Nowadays the importance of Extragalactic Background Light (EBL) becomes evident. Interaction with high energy EBL photons results in photo-disintegration of nuclei at low energies, while in pair-production energy losses and photo-disintegration at highest energies, CMB radiation dominates. Moreover, as recent accurate calculations show the PAO spectrum steepening at highest energies may be explained not only by nuclei interactions. It may be also produced as a result of a decreasing acceleration efficiency in the vicinity of the maximum energy $E_{\text{max}}$ that sources can provide (for reviews see [26]). The HiRes and TA data, in favour of proton composition, and the PAO data, in favour of nuclei composition, are further discussed in sections 2.3 and 2.4.

The GZK cutoff and pair-production dip are signatures of protons as primary particles. However, the direct measurement of mass composition is needed for consistency of the whole picture. The most reliable method to measure the mass composition nowadays is given by determination of the depth in the
atmosphere $X_{\text{max}}$ where the extensive air shower (EAS) reaches maximum and the distribution of $X_{\text{max}}$ over average value given by RMS($X_{\text{max}}$). The data of HiRes [6] and TA [27] show the proton-dominant mass composition at energy $E \gtrsim 1$ EeV in accordance with pair-production dip and GZK cutoff, while PAO data show nuclei mass composition with steadily increasing mass number $A$ at $E \gtrsim 3$ EeV, which practically reaches Iron at $E \sim 35$ EeV. This discrepancy of observational data makes us to study two different scenarios with (almost) pure proton composition, based on HiRes and TA data, and Auger-based scenario with steadily heavier mass composition at increasing energy. Four phenomenological models will be considered. The distinctive feature which characterizes each of them is energy of transition from Galactic to extragalactic cosmic rays. The main prediction is the mass composition and energy spectrum.

In the ankle models [28]–[35] it is assumed that the transition occurs at the flat part of the observed spectrum in the energy interval $E_{\text{trans}} \sim (3–10)$ EeV. The transition energy is given by the intersection of a flat extragalactic spectrum and a very steep galactic one. In the majority of ankle models the extragalactic component is assumed to be pure proton, while the galactic one should be naturally represented by Iron nuclei at energies above the Iron knee. These models predict a transition from an Iron-dominated composition to a proton-dominated one at the ankle energy.

In the mixed composition model [36] it is assumed that the extragalactic component consists of nuclei of various types. Thus transition here occurs from Iron to lighter nuclei of mixed composition; it can occur at the ankle or nearby it.

In the dip model the transition begins at the second knee and is completed at the beginning of the dip, at $E \approx 1$ EeV. The ankle in this model appears as an intrinsic part of the dip. Like in the ankle model, the transition here also occurs as an intersection of the flat extragalactic component (this flatness is especially prominent in the case of diffusive propagation) with the steep Galactic spectrum. In contrast to the ankle and mixed composition models, the dip model predicts an almost pure proton composition above $E \approx 1$ EeV and a pure Iron composition below this energy.

The Auger-based models are build for explanation of PAO data: energy spectrum [37] and mass composition [38] with proton or Helium dominance at $(1–3)$ EeV and with nuclei at higher energies with steadily increasing atomic number $A$ with energy. Transition from Galactic to extragalactic CRs occurs at the ankle.

We discuss in this presentation the status of these models.

2. SIGNATURES OF PROTON PROPAGATION THROUGH CMB

Propagating through CMB, UHE protons undergo two interactions: photo-pion production $p + \gamma_{\text{cmb}} \rightarrow N + \pi$ and $e^+ e^-$ production $p + \gamma_{\text{cmb}} \rightarrow p + e^+ + e^-$. As a result, the proton spectrum is distorted: due to the first interaction it obtains a sharp steepening called GZK cutoff and due to the second one - shallow deepening, called dip. Both features depend not only on interactions but also on model-dependent quantities, e.g. on modes of propagation (diffusion or rectilinear propagation), on cosmological evolution of the sources, on source separation etc. These model-dependent distortions are especially strong for GZK feature.

The main strategy of this presentation as well as of works [16–18] is to distinguish the interaction signatures from the model-dependent ones.

This is possible to do using the modification factor $\eta(E)$ [14], some kind of theoretical spectrum, in which model-dependent features are suppressed or absent. For this aim we use the calculations which involves only one free parameter. One naturally expects that the calculated interaction signature in terms of modification factor cannot have the agreement with observations with good $\chi^2$, because the observational data include the model-dependent features described by many parameters, such as cosmological evolution of the sources, source separation etc. One free parameter is not enough to describe 4–5 different experiments with about 20 energy bins in each. As the next step we perform the model-dependent calculations which necessarily include many free parameters improving further
the agreement. This analysis should be done in terms of usual \( E^3 J(E) \) spectrum, where the model-dependent features are not suppressed.

However, the Nature has been more kind to us than we expected. The dip, in terms of modification factor with one free physical parameter (interaction-signature description) gave very good \( \chi^2 \) agreement with observations of four experiments [39]: Yakutsk, AGASA, HiRes and Telescope Array (see section 2.1). The comparison with PAO data has a different story. Comparison in terms of modification factor with PAO observational data from ICRC 2007 (Merida) had good enough \( \chi^2 \) (see [40]). However, with increasing statistics the agreement became worse, and comparison of modification factor with PAO data 2010 – 2001 has bad \( \chi^2 \). It could be that for the difference in very small error bars the model-dependent effects are responsible. Indeed, as demonstrated in section 2.2 the 22% shift of PAO energy scale and cosmological evolution make the PAO spectrum in terms of \( \chi^2 \) fit for its definition, \( \chi^2 \). This analysis should be done in terms of usual observational data includes only two free parameters: exponent of the power-law generation spectrum \( g \), and separation within 1–50 Mpc, local source overdensity or deficit etc. The dip modification factor is modified strongly by presence of nuclei (\( \gtrsim 15\% \)). Modification factor for GZK feature is changing stronger.

Theoretical modification factors calculated for different source generation indices \( \gamma_g \) are presented in Fig. 1. If one includes in the calculation of \( J_p(E) \) only adiabatic energy losses, then, according to its definition, \( \eta(E) = 1 \) (dash-dot line in Fig. 1). When \( e^+e^- \) -production is additionally included, one obtains spectrum \( \eta(E) \) shown in Fig. 1 by the curves labeled as \( \eta_{ee} \). With the pion photo-production process being also included, the GZK feature (curves “total”) appears. The observable part of the dip extends from the beginning of the GZK cutoff at \( E \approx 40 \) EeV down to \( E \approx 1 \) EeV, where \( \eta \approx 1 \). It has two flattenings: one at energy \( E_b \approx 10 \) EeV and the other at \( E_b \approx 1 \) EeV. The former automatically produces the ankle (see Fig. 2) and the latter provides an intersection of the flat extragalactic spectrum at \( E \leq 1 \) EeV with the steeper Galactic one.

We discussed above the theoretical modification factor. The observed modification factor, according to definition, is given by the ratio of the observed flux \( J_{obs}(E) \) and unmodified spectrum \( J_{unn}(E) \propto E^{-\gamma_e} \), defined up to normalization as: \( \eta_{obs} \propto J_{obs}(E)/E^{-\gamma_e} \). Here \( \gamma_g \) is the exponent of the generation spectrum \( Q_{gen}(E_g) \propto E_g^{-\gamma_g} \) in terms of initial proton energies \( E_g \). Fig. 2 shows that both the pair production dip and the beginning of the GZK cutoff up to 80 EeV are well confirmed by experimental data [39] of Akeno-AGASA, HiRes, Yakutsk and TA. The comparison of the theoretical dip with observational data includes only two free parameters: exponent of the power-law generation spectrum \( \gamma_g \) (the best fit corresponds to \( \gamma_g = 2.6 \pm 2.7 \)) and the normalization constant to fit the \( e^+e^- \) -production dip to the measured flux. The number of energy bins in the different experiments is 20–22. The fit is characterized by \( \chi^2/d.o.f. = 1.0–1.2 \) for AGASA, HiRes and Yakutsk data. This is a very good fit for signature (see beginning of this section). For this fit we used the modification factor without
Figure 1. Modification factors for two generation indices $\gamma_g = 2.7$ and 2.0. The dotted curve shows $\eta_{ee}$ when only adiabatic and pair-production energy losses are included. The solid and dashed curves include also pion-production losses.

As was explained above, using a model approach with additional three parameters describing the cosmological evolution one can further improve the agreement. In Fig. 2 one can see that at $E \lesssim 0.6$ EeV the experimental modification factor, as measured by Akeno and HiRes, exceeds the theoretical modification factor. Since by definition the modification factor must be less than one, this excess signals the appearance of a new component of cosmic rays at $E < E_{tr} \approx 0.6$ EeV, which can be nothing else but the Galactic cosmic rays. This interpretation is confirmed by transition of heavy component to the protons in the upper-left panel of Fig. 5, that with good accuracy occurs at the same energy. Thus, according to HiRes data the transition from extragalactic to Galactic cosmic rays, occurs at energy $E_{tr} \sim 0.6$ EeV and is accomplished at $E \sim E_b \approx 1$ EeV (see upper-left panel in Fig. 5 as example).

2.2 Pair-production dip as energy calibrator

The energy position of pair-production dip is rigidly fixed by interaction with CMB and thus it can serve as energy calibrator for the detectors.

As we already mentioned, it is difficult to expect that in terms of the modification factor the dip described by one free physical parameter can fit the observational data with minimum $\chi^2$. One can shift the observed energy bins by the recalibration factor $\lambda_{cal}$, within the systematic error of observations, to minimize $\chi^2$ [17]. We shall refer to this procedure as ‘recalibration of energy scale’.

We discuss first the dip in PAO spectrum [37] presented by the filled boxes in the left panel of Fig. 3. As it was already mentioned, because of very small statistical error bars it has too large $\chi^2$ in comparison with pair-production dip terms of modification factor. We shall use then the model-dependent method in terms of $E^3 J(E)$ including the cosmological evolution $(1+z)^m$ up to $z_{max}$ as shown in the left panel of Fig. 3. Using two more free parameters $m$ and $z_{max}$ we can reach better agreement with the modified shape of the dip shown the solid curve in Fig. 3. Now we can shift the PAO energy bins by factor $\lambda_{cal}$ reaching the minimum $\chi^2$. For this $\lambda_{cal} = 1.22$ is needed. As a result we obtain picture shown in the right panel of Fig. 3. We obtained not only the excellent agreement with the shape of the theoretical
pair-production dip (solid curve) but also the good agreement with absolute fluxes of HiRes and TA. Note that disagreement with GZK cutoff remains for the three energy bins in energy interval 35–52 EeV.

Recalibration with help of pair-production dip for all five detectors (HiRes, Telescope Array, PAO, AGASA and Yakutsk) is shown in Fig. 4. Recalibration factor $\lambda_{\text{cal}} = 1$ for HiRes/TA is based on the scale factor which correctly describes the pair-production dip and GZK cutoff in differential and integral ($E_{1/2}$) spectra.

2.3 GZK cutoff in HiRes and Telescope Array data

The two largest Extensive Air Shower (EAS) detectors, HiRes [9] and Pierre Auger Observatory [11] have observed a sharp steepening in the UHECR spectrum at $E \gtrsim (30–50)$ EeV. Both collaborations claimed that the observed steepening is consistent with the GZK cutoff. But as a matter of fact, there is a dramatic conflict between these two results, which still leaves the problem open.

In this subsection we analyze data of the HiRes which provide a strong evidence in favour of the GZK cutoff. These data are supported also by the TA data [10]. The data of PAO will be considered in the next subsection.

To interpret convincingly the spectrum steepening as the GZK cutoff one must prove that (i) energy scale of the cutoff and its shape correspond to theoretical predictions and (ii) the measured mass composition is strongly dominated by protons. In HiRes the mass composition is determined from

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**Figure 2.** The predicted pair-production dip in comparison with Akeno-AGASA, HiRes, Yakutsk and Telescope Array data [39]. All these experiments confirm the dip behavior with good accuracy, including also the data of Fly’s Eye [39] (not presented here).
Figure 3. Left panel: comparison of the PAO energy spectrum (filled boxes) with the HiRes and TA data fitted by theoretical pair-production dip (solid curve). Right panel: spectra after energy recalibration of the PAO data with \( \lambda_{\text{cal}} = 1.22 \) (see the text).

Figure 4. Left panel: original fluxes from all detectors (fluxes from HiRes and TA are approximately the same). Right panel: spectra after energy recalibration by pair-production dip: \( \lambda_{\text{cal}} = 1 \) for HiRes/TA, \( \lambda_{\text{cal}} = 1.22 \) for PAO, \( \lambda_{\text{cal}} = 0.75 \) for AGASA and \( \lambda_{\text{cal}} = 0.625 \) for Yakutsk.

The integral energy spectrum of UHE protons, \( J_p(>E) \), has another specific characteristic of the GZK cutoff, the energy \( E_{1/2} \) [14]. It is based on the observation that the calculated integral spectrum below 50 EeV is well approximated by a power-law function: \( J_p(>E) \propto E^{-\tilde{\gamma}} \). At high energy this spectrum is steepening due to the GZK effect. The energy where this steep part of the spectrum equals to the half of its power-law extrapolation, \( J_p(>E) = K E^{-\tilde{\gamma}} \), defines the value of \( E_{1/2} \). This quantity is found to be practically model-independent; it equals to \( E_{1/2} = 10^{19.72} \) eV \( \approx 52.5 \) EeV [14]. Fig. 5 demonstrates how the HiRes collaboration found \( E_{1/2} \) from observational data [44]. The ratio of the measured integral spectrum \( J(>E) \) and the low-energy power-law approximation \( K E^{-\tilde{\gamma}} \) was plotted as a function of energy. This ratio is practically constant in the energy interval 0.3–40 EeV, indicating that...
the power-law approximation is a good fit, indeed. At higher energy the ratio falls down and intersects the horizontal line 0.5 at the energy defined as $E_{1/2}$. It results in $E_{1/2} = 10^{19.73 \pm 0.07}$ eV, in an excellent agreement with the predicted value.

Thus, one may conclude that the HiRes data presented in Fig. 5 indicate the proton-dominated chemical composition and the presence of the GZK cutoff in both differential and integral spectra. The conclusion about proton composition is further supported by the recent TA data [27].

### 2.4 PAO data: Energy spectrum and mass composition

In subsection 2.2 we demonstrated that the dip shape, as observed by PAO, can agree after recalibration with energy spectra of HiRes/TA and other detectors (see Figs. 3 and 4). The coincidence of the PAO and HiRes/TA spectra is related to low energy part of the energy spectrum in the right panel of Fig. 3. At higher energies statistical uncertainties are too large to distinguish between the spectra.

While the HiRes and TA spectra are compatible with the GZK cutoff, the Auger spectrum is not. The steepening in the upscaled PAO spectrum starts at energy $E \lesssim 40$ EeV, lower than $E_{\text{GZK}} \simeq 50$ EeV, and in three successive energy bins in the interval 35–52 EeV the PAO flux is significantly lower than one predicted for the GZK shape as shown in the right panel of Fig. 3. We could not reconcile the PAO cutoff shape with the GZK behavior by including in the calculations different generation indices $\gamma_g$, evolution regimes, low acceleration maximum energy $E_{\text{max}}$, local overdensity of sources etc.
Figure 6. Left panel: Auger data \([X_{\text{max}}]\) as function of the energy (left panel) and for RMS\((X_{\text{max}})\), the width of the distribution over \(X_{\text{max}}\) (right panel). The calculated values for protons and Iron are given according to QGSJET01 [41] and QGSJET II [42] models. One can see from the right panel that RMS distribution becomes more narrow with increasing energy which implies a progressively heavier mass composition.

This disagreement is quite natural for the PAO mass composition data which, in contrast to HiRes and TA, show strong dominance of nuclei (see Fig. 6). A steepening in the end of the of the nuclei spectrum, as calculations show, is quite different from that of protons (GZK cutoff). The most reliable data on mass composition is given by elongation curve \(X_{\text{max}}(E)\) and especially by RMS\((X_{\text{max}}(E))\). In the Auger data the latter steadily decreases with energy and approaches the Iron value at \(E \approx 35\) EeV. Low RMS, i.e. small fluctuations, is a typical and reliable feature of the heavy nuclei composition. These data are further strengthened by other PAO measurements provided by surface detectors. They allow to extract two other mass-composition dependent quantities: the atmospheric depth \(\langle X_{\text{atm}}\rangle\), where muon-production rate reaches maximum, and maximum zenith angle \(\vartheta_{\text{max}}\) determined by the signal rise-time in surface Cerenkov detectors. Measurements of both quantities confirm the heavy mass composition and its dependence on energy obtained with the help of \(\langle X_{\text{max}}\rangle\) and RMS\((X_{\text{max}})\), [45] and [46], respectively. The soon expected data on muon flux from the Auger Muon and Infill Ground Array (AMIGA) [47] will further clarify the mass composition.

Our further analysis of the Auger spectrum and mass composition is based on the following two observations:

(i) According to the HiRes (Fig. 5) and PAO (Fig. 6) data, the observed primaries at energy (1–3) EeV are predominantly protons or nuclei not heavier than Helium. These particles cannot be galactic, otherwise, as MC simulations [48] show, galactic anisotropy would be too large. Then the ankle in the PAO data is not a transition from galactic to extragalactic cosmic rays, but transition from extragalactic protons/Helium to extragalactic nuclei. Transition from galactic to extragalactic CRs occurs thus at lower energies, most probably at the second knee.

(ii) The particles at higher energies are extragalactic nuclei with the charge number \(Z\) increasing with energy. This observation is naturally explained by rigidity dependent acceleration in the sources \(E_{\text{max}}^i = Z_i \times E_p^{\text{max}}\), since at each energy \(E = Z E_p^{\text{max}}\) the contribution of nuclei with smaller \(Z' < Z\) vanishes.

It was demonstrated in [49] that to avoid a proton dominance at the highest energies, one must assume that the maximum energy of the accelerated protons is limited, \(E_p^{\text{max}} \lesssim (4–10)\) EeV. This conclusion is valid for a large range of generation indices, \(\gamma_p \sim 2.0–2.8\), and for a wide range of cosmological evolution parameters. The calculated proton and nuclei energy spectra for \(\gamma_p = 2.0, E_{\text{max}} = Z \times 4\) EeV and without cosmological evolution are shown in Fig. 7. In the left panel the two component model (protons and Iron) is presented. In the right panel intermediate primary nuclei are included in the framework of the diffusive propagation through intergalactic magnetic fields (see [49] for
Figure 7. *Left panel:* energy spectrum in the two-component model with protons and Iron nuclei for homogeneous distribution of sources and with $\gamma_g = 2.0$ and $E_{\text{max}} = 4 \, \text{EeV}$. *Right panel:* as in left panel but with a diffusion cutoff. The gap is expected to be filled by intermediate mass nuclei.

details). However, it is a problem to explain simultaneously both the spectrum and the mass composition of the PAO. This model is called “disappointing” because of lack of many signatures predicted in proton-dominated models, such as cosmogenic neutrino production and correlation of CR arrival directions with distant sources.

The similar model is considered in [50] (see Fig. 4 there). Like in [49] the proton component with $E_{\text{max}} = 4 \, \text{EeV}$ is introduced and rigidity-dependent acceleration is considered. The more detailed calculations including the secondary nuclei are performed for Iron-enriched source spectrum. The calculated spectrum agrees well with that of PAO at $E \gtrsim 3 \, \text{EeV}$.

More detailed calculations are performed in [51]. For Iron or Silicon as the accelerated nuclei, and very flat generation spectrum with $\gamma_g < 2.0$, the energy spectrum and mass composition of the produced nuclei are calculated for rectilinear and diffusive propagation. In some cases the agreement with Auger data is reached for energy spectrum and RMS($E$) (agreement with elongation curve is worse). The rigidity-dependent acceleration is not assumed and problem with proton/Helium component at $(1–3) \, \text{EeV}$ is not discussed. The presence of nearby sources is emphasized as a general feature.

3. THREE TRANSITION MODELS

In this section we discuss three models of transition from Galactic to extragalactic CRs: ankle, dip and mixed composition models. One feature is common for all of them: the transition is described as an intersection of a steep Galactic spectrum with a flat extragalactic one. The agreement with the SM for GCR is one more criterion which these models have to respect. According to the Standard Model, the benchmark of the end of GCR is given by the Iron knee at energy $E_{\text{Fe}} \approx 80 \, \text{PeV}$ and at $E > E_{\text{Fe}}$ it has an exponential cutoff.

Motivated by the interpretation of the ankle as the transition to extragalactic CR at $E_{\text{tr}} \sim (3–10) \, \text{EeV}$, one has to assume [30–32] an additional component of GCR accelerated to energies much beyond the Iron knee.

Observational data which have the power either to confirm or to reject each transition model include energy spectrum, elongation curve ($X_{\text{max}}(E)$), RMS($X_{\text{max}}$) and anisotropy. Below these models are discussed in the historical succession of appearance: ankle, dip and mixed composition.

3.1 Ankle model

This is the traditional model based on the interpretation of the ankle as the spectrum feature where transition occurs (see e.g. [28]–[35]). In fact, this is a very natural model since transition occurs because the extragalactic component is very hard. This component is assumed to have a pure proton
Figure 8. The calculated elongation curves $\langle X_{\text{max}} \rangle (E)$ for the dip model (two left panels) and ankle model (right panels). The calculated curves $\langle X_{\text{max}} \rangle (E)$ are shown by the thick solid lines for QGSJET01 [41] model of interaction, by the thick dashed lines for QGSJET-II [42], and by dotted lines for SIBYLL [53]. The data points are measurements of HiRes-Mia (filled triangles), HiRes and PAO (both filled boxes). The PAO data in upper panels with systematic errors, shown by the thin curves, are taken from [54]. The lines “p” and “Fe” present the elongation curves for proton and Iron which are used for calculations of the model elongation curves in each panel. For PAO data they are theoretical curves, for HiRes they include cuts, detector’s properties etc. and are taken from curves “iron” and “proton” in the upper-left panel of Fig. 5. As the main result of these plots one may notice the great discrepancy of the ankle model with the data.

composition with a flat generation spectrum $Q_{\text{extr.p}} \propto E^{-2}$ valid for non-relativistic shock acceleration. Energy losses modify the spectrum insignificantly at $E \lesssim 40$ EeV. The beginning of the ankle at $E_{\text{obs}} \sim 4$ EeV corresponds to the energy where fluxes of Galactic and extragalactic CRs get equal. Thus, the Galactic CRs should be presented by an additional component accelerated up to energy by factor 30–40 times higher than the maximum energy in the Standard Model. In the majority of ankle models, e.g. [30, 31, 34, 35], the large fraction of the observed cosmic rays has a Galactic origin at $E \gtrsim 10$ EeV. To facilitate the acceleration problem one should assume a heavy-nuclei composition of the new component.

Another problem of the ankle model is the contradiction with the measured average depth of EAS maximum, $\langle X_{\text{max}} \rangle (E)$, in the energy range (1–4) EeV. While all data, including both HiRes and PAO, show proton or light nuclei composition here, the ankle model needs a heavy Galactic component, predicting too small $\langle X_{\text{max}} \rangle (E)$ in contradiction with observations (see the right panels of Fig. 8 and right panel of Fig. 4 in [52]). This contradiction is found also in [48] and [36].

Another contradiction in the ankle model is given by observed proton/Helium composition at (1–3) EeV. Since this energy interval is below the ankle, i.e. has galactic origin, anisotropy there should be too high [48]. One may conclude that ankle model is excluded or very strongly disfavoured.
3.2 Dip model

The dip model is based on the assumption that UHECRs at \( E \gtrsim 1 \text{ PeV} \) are mostly extragalactic protons. This assumption is confirmed by the HiRes and TA data (mass composition and observation of pair-production dip and GZK cutoff), but contradicts to PAO mass composition data. The transition from galactic to extragalactic component begins at the second dip and finishes at \( E \sim 1 \text{ PeV} \) in good agreement with SM of Galactic CRs.

The basic features of the dip model are as follows [16–18]:

(i) The sources are AGN [55] with a neutron mechanism of particle escape [56, 57] which provides a pure proton generation spectrum.

(ii) The source generation spectrum has a usual shock-acceleration form \( q(E) \propto (E^{-2} - E^{-2.3}) \), but generation rate per unit comoving volume at high energy can be \( Q(E) \propto E^{-\gamma_g} \) with \( \gamma_g = 2.6–2.7 \) due to distribution of the sources over the maximum energy of acceleration \( n_s(E_{\text{max}}) \) [58].

(iii) The generation index \( \gamma_g = 2.6–2.7 \) is the main fitting parameter (see subsection 2.1). The cosmological evolution of the sources can be easily included, affecting mostly the low energy part of the spectrum. Inclusion of additional parameters allows to improve the fit. In particular, in [17] the spectrum was calculated with an account for cosmological evolution of AGN as it follows from X-ray observations.

The confirmation of the dip model follows from: (i) agreement of the dip energy spectrum with observations (see Fig. 2), (ii) equality of all measured fluxes after the dip-based energy recalibration (see Fig. 4) and (iii) agreement of \( \langle X_{\text{max}} \rangle(E) \) with the bulk of observations in the left panels of Fig. 8.

At present the dip model is confirmed by the data of HiRes and TA by strong proton-dominance at \( E > 1 \text{ PeV} \), and is in contradiction with the Auger measurements of \( \langle X_{\text{max}} \rangle(E) \) and RMS at \( E > 4 \text{ PeV} \). The key observation to accept or reject the dip model is the chemical composition of UHECR at \( E > 1 \text{ PeV} \). In the case of a substantial admixture of nuclei in the spectrum (>20%) the dip model should be rejected.

3.3 Mixed composition model

The main concept of the mixed composition model (see Allard et al. [36]) is based on the argument that any acceleration mechanism operating in gas involves different species of nuclei in acceleration process and thus the primary flux must have a mixed composition.

The basic features of the mixed composition model are as follows [36]: (i) In its basic versions [36], the source composition of extragalactic CRs is assumed to be almost the same as for Galactic CRs, with protons and Helium being the dominant components. (ii) The source energy spectra are taken as power-law with a generation index \( \gamma_g = 2.1–2.3 \), with the maximum acceleration energy assumed to be rigidity dependent, and with cosmological evolution of the sources considered to be in a wide range of regimes. (iii) The sources usually are assumed to be distributed homogeneously in the universe. The propagation is studied using Monte Carlo with nuclei photo-disintegration on the CMB and EBL. (iv) At a first glance one may expect that a large number of free parameters, such as generation index, parameters of cosmological evolution and coefficients of source nuclei composition, can provide a broad variety of observed mass compositions and spectra. However, as it was demonstrated in [36], the predictions are very much constrained due to photo-disintegration of nuclei on EBL and CMB radiations. (v) The basic physics phenomena and their results are as follows. Generically in the mixed models the mass composition becomes lighter at \( E > 10 \text{ PeV} \), because intermediate and heavy nuclei are destroyed by the EBL photons while protons survive. In principle this situation may change only above 50 PeV, when GZK cutoff in the proton spectrum appears, while heavy nuclei, e.g. Iron, are still not photo-disintegrated by the CMB photons and may dominate. In realistic cases the dominant component in mixed models are protons. (vi) Transition from Galactic to extragalactic component in the mixed models depends on the choice of parameters. In most models transition occurs at the ankle, see Allard et al. in [36]. However,
in the conceptually important paper by Allard, Olinto, Parizot (2007) from [36] it was emphasized that for strong source evolution and flat generation spectra the intersection of Galactic and extragalactic components occurs between 0.5 EeV and 1 EeV, i.e. at the second knee, as in the dip model.

The dominance of protons was the reason why the \( \langle X_{\text{max}} \rangle (E) \) predicted by mixed composition models is in a better agreement with HiRes data than with PAO data. The observations of PAO show that mass composition becomes heavier with increasing energy, and thus the existing calculations in the framework of mixed models agree better with the HiRes data.

However, with the recent proposal [59] the power of the mixed composition model for fitting the PAO data may change due to a possible enhancement of the heavy nuclei production.

4. CONCLUSIONS

In this paper we limited our consideration by the models for diffuse fluxes of UHECR. We will touch the problem of the produced neutrinos and detection of sources only shortly in the end of this section. The traditional interest for diffuse fluxes is given by the highest energies, namely by the search for the GZK cutoff. Its unambiguous discovery, however, means only that primaries are protons and exotic solutions are excluded. The low-energy part of extragalactic CRs can give a key information on the existence of pair-production dip, on propagation of CRs in extragalactic magnetic fields and shed more light on the end of Galactic CRs.

Therefore, the experimental studies in the transition region (0.1–10) EeV are of paramount importance in this field of research, with the mass composition measured by different methods being probably most important task.

There are four working detectors which cover partially the above-mentioned region: KASCADE-Grande [60], Tunka [61], Yakutsk [62] and IceTop/IceCube [63]. There are also projects to extend the observations of Telescope Array and PAO to low energies, (0.1–1) EeV at TALE [64] and at LE-Auger [65]. The Auger detector has a great potential to explore the low-energy region of the UHECR spectrum. At present there are already two new detectors at PAO collecting data at this energy; High Elevation Auger Telescope (HEAT) [66], detecting the fluorescent light at higher elevation angles; and Auger Muons and Infill Ground Array (AMIGA) [47], for the detection of the EAS muon component. These detectors, together with TALE, Tunka, Yakutsk and IceCube/IceTop will provide information on all radiations from EAS, including fluorescent and Cherenkov light, muons and radio radiation. One may expect that in this way the present controversy between the mass compositions in the HiRes and Auger detectors will be unambiguously solved. The recent measurement [45, 46] of the muon-production depth \( X_{\text{max}} \) and maximum zenith angle \( \theta_{\text{max}} \) by on-ground Auger detectors is an important step in this direction.

At the low-energy end of the UHECR the energy spectra are measured with an unprecedented accuracy for cosmic ray physics. However, in fact even in experiments with the same technique, like HiRes and Auger, the energy scales are different due to systematic errors. However, there is a physical ‘standard candle’ for the detector energy calibration, given by the fixed energy position of the pair-production dip. The recalibration factor \( \lambda_{\text{cal}} \) can be found by the spectrum shift to the energy at which agreement between observed and predicted dips is the best (see [17, 18] and Blümmer et al. in [26]).

There are three models of transition: ankle, dip and mixed composition one. The ankle model is excluded or severely disfavoured by proton or Helium composition at energy (1–3) EeV, i.e. below the ankle, where the particles have Galactic origin. The mass composition at these energies will be reliably measured by future low-energy detectors. However, the argument against the ankle model obtained from Fig. 8 remains to be valid independently from mass composition at (1–3) EeV, unless it is very heavy.

A search for UHE neutrinos UHECR sources is outside the scope of this review. However, a few remarks may be useful here.
In some particular dip models (see subsection 3.2) with proton-dominated mass composition the cosmogenic neutrinos can be detectable. The flux of cosmogenic neutrinos are severely constrained by the electro-magnetic cascade upper limit [67] and only in extreme cases [68, 69] it can be detectable, e.g. by JEM-EUSO [70]. Another case of flux detectable by Ice-Cube at smaller energies $E \sim 10^{15}$ eV is given by cosmogenic neutrinos produced at ‘bright phase’ [71]. UHE neutrinos can in principle indicate directions to the sources.

Even in the case when heavy nuclei dominate in the source radiation, the protons are accelerated there too, and even small produced flux can be detected from a nearby source. However, such possibility not always exists. For example in the disappointing model [49] for interpretation of Auger results the maximum energy of protons $E_{\text{max}} \sim 4$ EeV is too small to reach rectilinearly detector from a source.

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UHECR 2012
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