Prediction of disease–gene–drug relationships following a differential network analysis

S Zickenrott¹, VE Angarica¹, BB Upadhyaya¹ and A del Sol*¹

Great efforts are being devoted to get a deeper understanding of disease-related dysregulations, which is central for introducing novel and more effective therapeutics in the clinics. However, most human diseases are highly multifactorial at the molecular level, involving dysregulation of multiple genes and interactions in gene regulatory networks. This issue hinders the elucidation of disease mechanism, including the identification of disease-causing genes and regulatory interactions. Most of current network-based approaches for the study of disease mechanisms do not take into account significant differences in gene regulatory network topology between healthy and disease phenotypes. Moreover, these approaches are not able to efficiently guide database search for connections between drugs, genes and diseases. We propose a differential network-based methodology for identifying candidate target genes and chemical compounds for reverting disease phenotypes. Our method relies on transcriptomics data to reconstruct gene regulatory networks corresponding to healthy and disease states separately. Further, it identifies candidate genes essential for triggering the reversion of the disease phenotype based on network stability determinants underlying differential gene expression. In addition, our method selects and ranks chemical compounds targeting these genes, which could be used as therapeutic interventions for complex diseases.

Cell Death and Disease (2016) 7, e2040; doi:10.1038/cddis.2015.393; published online 14 January 2016

The availability of reliable methodologies for generating iPSC-derived cells¹,² (induced pluripotent stem cells) has contributed to the establishment of disease modeling as a very promising approach for studying the molecular basis of disease onset and progression. Moreover, the possibility of producing patient-specific iPSC-derived cells from individuals with disease-relevant mutations offers an advantageous in vitro system for the study of pathogenesis and performing drug screening in differentiated human cell types.³ However, the multifactorial nature of many human diseases, which are characterized by the dysregulation of multiple genes and interactions in gene regulatory networks (GRNs)⁴–⁶ significantly hampers our understanding of molecular mechanisms related to the disease pathology. As a result, the rate at which novel drug candidates can be translated into effective therapies in the clinic is rather low.⁷,⁸

In the past years, the large-scale generation of high-throughput biological data has enabled the construction of complex interaction networks that provide a new framework for gaining a systems level understanding of disease mechanisms.⁹ These network models have been useful for predicting disease-related genes based on the analysis of different topological characteristics, such as node connectivity,¹⁰ or gene–gene interaction tendency in specific tissues.¹² Disease-gene associations have also been predicted based on the identification of network neighbors of disease-related genes,¹³–¹⁵ or by predicting disease-related subnetworks.¹⁶–¹⁸ In other approaches, cellular phenotypes are represented as attractors—that is, stable steady states—in the gene expression landscape,¹⁹ and phenotypic transitions are modeled by identifying nodes destabilizing these attractors.²⁰–²² This rationale has been used to model disease onset and progression as transitions between attractor states, in which disease perturbations, such as chemical compounds or mutations, can cause a switch from a healthy to a disease attractor state.²³,²⁴

An alternative approach increasingly used explores functional connections between drugs, genes and diseases, involving the development of databases and tools integrating bioactivity of chemical compounds, chemical perturbation experiments and drug response at the cellular, tissue or organism levels.²⁵–²⁸ In particular, some of these resources have been developed for connecting drugs and diseases based on gene signatures²⁹–³¹ — for example, differentially expressed genes between disease and healthy phenotypes. For example, the Connectivity Map (CMap)³⁰,³¹ constitutes a widely used database of gene expression profiles from cultured human cancer cells perturbed with chemicals and genetic reagents. It has been successfully applied for predicting drug effects and mode of action in different human diseases.³²–³⁵ However, following this approach disregards the underlying gene regulatory mechanisms. Network pharmacology strategies attempt to address this problem and identify genes whose perturbations could result in a desired
Predicting disease-gene-drug relationships
S Zickenrott et al

Table 1 ChiP-Seq validation of phenotype-specific network inference algorithm

|           | HepG2/GM | HepG2/H1 | HepG2/K562 | GM/H1 | GM/K562 | H1/K562 |
|-----------|----------|----------|------------|-------|---------|---------|
| Raw       | 92       | 36       | 122        | 20    | 74      | 2       |
| Pruned    | 86       | 30       | 111        | 13    | 71      | 2       |
| Retained (in %) | 93.5     | 83.3     | 91         | 65    | 95.9    | —       |

For six different examples, we compared the number of initially contained interactions from ChiP-Seq (Raw) to those contained in the phenotype-specific networks. On average the network inference algorithm retains 86.6% of ChiP-Seq interactions in the contextualized networks.

therapeutic outcome. This guided rationale for drug prediction is of great importance as previous studies suggest that only ~15% of network nodes can be chemically tractable with small-molecule compounds. Moreover, molecular network robustness may often counteract drug action on single targets, thus preventing major changes at a systems level. Thus, network pharmacology methodologies are promising for the identification of optimal combinations of multiple proteins in the network whose perturbation could revert a disease state.

Nevertheless, current network and gene signature-based approaches for identifying disease-related genes and drug–disease associations have important limitations. In particular, network-based methods rely on a unique network topology while there are compelling evidences suggesting that different cellular phenotypes, such as healthy and disease states, are characterized by fairly different GRN topologies, leaving these methods unable to identify differential regulatory mechanisms leading to a disease pathology. Furthermore, gene signature-based methods, such as the CMap, have some important shortcomings for the selection of the right subset of genes composing a signature. Recently, new methods have been proposed to improve gene signature analysis assuming independence between the expression of different genes, leading to more reliable drug–disease connections and drug–disease connections. However, a detailed analysis of gene–gene interaction networks in a specific phenotype is generally neglected in these approaches. Moreover, to our knowledge there are no approaches combining information on perturbation of cellular phenotypes with a thorough differential network-based analysis for identifying disease–gene–drug relationships. In addition, strategies for predicting multitarget drugs are scarce and there is a lack of a robust set of design tools to routinely apply these multitarget approaches.

In this paper, we introduce a novel network-based approach for predicting target genes and bioactive compounds that could revert disease phenotypes. Our method relies on the reconstruction of GRNs corresponding to disease and healthy phenotypes by compiling gene interactions from literature. Further, it performs a differential network analysis for identifying gene targets and drugs that could induce the transition from disease to healthy phenotypes. Validation of our method with perturbation data from the CMap shows that in most cases our predictions of drugable genes is in good agreement with the experimental data. Finally, our method was used to make predictions of disease-related genes and bioactive compounds in three different disease models, which have not been extensively studied. Thus, we believe that the method presented here can be useful in the identification of disease–gene–drug relationships, and therefore in guiding experimentalists in the design of effective therapeutic strategies for treating human diseases.

Results
Network reconstruction and differential network analysis. Network-based models of GRNs constitute an important tool for disease modeling, aiming at identifying disease-causing genes. Experimental studies suggest that the regulatory impairments leading to disease pathology are associated with different GRN topologies, underlying the phenotypic differences between healthy and disease states. Thus, differential network modeling is essential for identifying differential regulatory network modules stabilizing the pathological expression pattern under study. In the approach presented here, our method infers phenotype-specific GRNs for disease and healthy states, starting from experimentally validated gene–gene interactions compiled from Thomson Reuters’ MetaCore database. To obtain contextualized GRNs, our method prunes literature interaction maps compiled in each case, including interactions occurring in different tissues and organisms, and at the same time infers the mode of action of interactions having unspecified effects (see Materials and Methods for details).

We validated the inference algorithm by assessing the enrichment of validated ChiP-Seq interactions before and after contextualization (see Materials and Methods for details). Our results for these benchmarking assays show that up to 89.6% of the ChiP-seq interactions are preserved in the contextualized networks (Table 1), which demonstrate that our method is able to reconstruct fairly reliable phenotype-specific GRNs (Supplementary File S1). Moreover, we observe a high variability in the ratio of phenotype-specific and common interactions between the two networks in these examples (Table 2), indicating that both phenotypes cannot be accurately modeled by considering a single GRN topology, thus highlighting the importance of a differential network analysis approach. We also performed a thorough comparison of our method with other methods available for network reconstruction of direct and signed GRNs using CellNOptR and SignetTrainer. In this comparison, we measured the enrichment in experimentally validated interactions in the reconstructed GRNs, as well as the agreement between the GRN models generated by each method and the phenotype-specific gene expression patterns in the 20
drugs to revert the disease phenotype. Enrichment analysis allow us to predict the most suitable methods for details). Combining simulation assays and enrichments between these networks to derive candidate target nants between these networks to derive candidate target genes, whose perturbations could revert the disease phenotype (see Materials and Methods for details). We analyzed GRN response to millions of combinations of target gene perturbations, in the following referred to as multitarget combinations, and ranked drugs according to the enrichment of their targets in these multitarget combinations (see Materials and Methods for details). At the same time, simulation assays were performed to study the effects of specific drugs on the system’s attractor (see Materials and Methods for details). Combining simulation assays and enrichment analysis allow us to predict the most suitable drugs to revert the disease phenotype.

Validation of the algorithm for inferring disease–gene–drug relationships. To show the applicability of our method for predicting genes and drugs triggering cellular phenotypic transitions, we selected six examples from the CMap, encompassing cellular gene expression changes upon chemical perturbation. These examples include the use of different chemical compounds such as celastrol+androgen, gedunin+androgen, celastrol, cobalt chloride, estradiol and genistein for treating LNCap or MCF7 cell lines. Following our methodology, we contextualized GRNs for the control and drug-induced phenotypes and assessed enrichment of the top-ranking drugs obtained from the CMap by means of simulated multitarget combinations (see Materials and Methods for details).

In all but one of the examples, we identified multitarget combinations able to revert at least 60% of the gene expression pattern (Supplementary Table S1). Furthermore, comparing the resulting enrichment distributions clearly identifies the drug inducing the phenotypical change in all cases (Table 3). Here, lower area under the curve (AUC) values correspond to better enrichment patterns, as the cumulative enrichment distribution functions are then lowly enriched in the worst multitarget combinations and highly enriched in the top-ranking ones. The deviation from the uniform AUC then provides insight into how much more specific the drugs are in comparison with an uninformative enrichment pattern (see Materials and Methods for details).

Table 2 Statistics of validation networks for the network inference algorithm

|                  | HepG2/Gm12878 | HepG2/H1-hESC | HepG2/K562 | Gm12878/H1-hESC | Gm12878/K562 | H1-hESC/K562 |
|------------------|--------------|--------------|------------|-----------------|-------------|-------------|
| Common           | 424          | 608          | 430        | 298             | 662         | 594         |
| Phenotype1 total | 530          | 824          | 520        | 324             | 999         | 859         |
| Phenotype1 specific | 106        | 216          | 90         | 26              | 337         | 265         |
| Phenotype1 ratio | 20.00%       | 26.20%       | 17.30%     | 8.00%           | 33.70%      | 30.80%      |
| Phenotype2 total | 508          | 707          | 498        | 323             | 819         | 720         |
| Phenotype2 specific | 84          | 99           | 68         | 25              | 157         | 126         |
| Phenotypes2 ratio | 16.50%      | 14.00%       | 13.70%     | 8.30%           | 19.20%      | 17.50%      |

For six different examples, the number of common and phenotype-specific interactions is dissected. The percentage of phenotype-specific variations marked between 8.0 and 33.7%, highlighting the necessity of a differential network approach to accurately represent two different phenotypes.

Table 3 Statistical comparison of simulated drugs in the validation examples

| Case          | Drug       | AUC       | Difference from AUC of uniform distribution |
|---------------|------------|-----------|---------------------------------------------|
| Celastrol+    | Celastrol+ | 12.645    | 25.61%                                      |
| androgen      | androgen   | 10.423    | 25.55%                                      |
| Gedunin+      | Gedunin+   | 14.628    | 5.62%                                       |
| androgen      | androgen   | 13.772    | 11.15%                                      |
| Estradiol     | Arachidonic acid | 18.683 | –0.99%                                      |
| Genistein     | Genistein  | 12.855    | 17.06%                                      |
| Estradiol     | Cobalt chloride | 14.628 | 5.62%                                       |
| Estradiol     | Estradiol  | 13.772    | 11.15%                                      |
| Estradiol     | Genistein  | 12.855    | 17.06%                                      |
| Estradiol     | Tacrolimus | 14.532    | 0.62%                                       |
| Cobalt chloride | Cobalt chloride | 4        | 27.27%                                      |
| Cobalt chloride | Cobalt chloride | 4        | 27.27%                                      |
| Cobalt chloride | Genistein   | 4.833     | 12.12%                                      |
| Cobalt chloride | Tretinoin   | 4.134     | 24.83%                                      |
| Cobalt chloride | Celastrol   | 19.776    | 15.85%                                      |
| Cobalt chloride | Genistein   | 21.943    | 0.66%                                       |
| Cobalt chloride | Whitalerin A | 24.471   | –0.41%                                      |

In the six drug-induced examples taken from the CMap, the area under the curve (AUC) of the cumulative enrichment distribution function is shown and compared against the AUC of a uniform distribution. Lower AUC values and higher difference from the uniform distribution indicate an enrichment of drug targets in multitarget combinations able to induce a higher change of the gene expression program. The most enriched drugs are highlighted in each case (bold) and agree with the experimentally induced drug.

benchmarking data sets analyzed (Supplementary Table S2.1 in Supplementary File S2). The results confirm that our method generates more accurate GRNs (94% compared with 48 and 88%) while showing higher enrichment in ChIP-Seq-validated interactions (94% compared with 58 and 83%).

After obtaining healthy and disease phenotype-specific GRNs, our methodology identifies common stability determinants between these networks to derive candidate target genes, whose perturbations could revert the disease phenotype (see Materials and Methods for details). We analyzed GRN response to millions of combinations of target gene perturbations, in the following referred to as multitarget combinations, and ranked drugs according to the enrichment of their targets in these multitarget combinations (see Materials and Methods for details). At the same time, simulation assays were performed to study the effects of specific drugs on the system’s attractor (see Materials and Methods for details). Combining simulation assays and enrichment analysis allow us to predict the most suitable drugs to revert the disease phenotype.
of RUNX1 (runt-related transcription factor 1), FOSL2 (FOS-like antigen 2), ASCL1 (achaete-scute family BHLH transcription factor 1) and SOX2 (SRY (sex determining region Y)-Box 2), which belong to network stability determinants (Supplementary Table S1 and Figure 2). Topological analysis of the contextualized control network reveals only four repressive interactions, so that the repression of a gene can only be modulated by the absence of any activator, explaining the poor change in the gene expression program upon perturbation (Figure 2). However, cobalt chloride is still identified as the most suitable drug to induce the phenotypical transition (Table 3). As can be seen in Figure 1 and Table 3, in general the top-ranking solutions predicted using our methodology are enriched in genes targeted by the drugs that were used to experimentally induce the phenotypic transition.

Figure 1  Results of drug-induced examples from the CMap. Violin plot of (a) celastrol, (b) cobalt chloride, (c) estradiol, (d) genistein, (e) celastrol+androgen and (f) gedunin+androgen showing the enrichment of drugs in the space of normalized gene expression changes resulting from simulated multitarget combinations. White dots represent the mean gene expression change of the simulated multitarget combinations underlined by the variance of the distribution (black bar). The dashed lines show the maximum enrichment score in percent for each drug in all of the cases. An optimal enrichment pattern corresponds to low scores in low normalized gene expression changes and high scores in high expression changes reflecting that the drug targets are specific to induce significant changes of the gene expression pattern. Application of cobalt chloride in (b) is an example of such optimal distributions.

Predicting candidate genes and drugs from disease-control studies. We applied our methodology to disease/control case studies, including rheumatoid arthritis in B cells and systemic lupus in B and CD4+ cells for identifying differential network determinants involved in stabilizing disease and healthy phenotypes, for predicting genes that could be perturbed to revert the disease phenotypes. Further, we gathered information from the Comparative Toxicogenomics Database\textsuperscript{46} to identify gene–drug mode of action to
propose candidates for perturbing the predicted target genes. Enrichment of the drugs was assessed by comparing the AUC of the cumulative enrichment distribution function and compared against the AUC of a uniform, uninformative enrichment distribution (see Materials and Methods for details). An overview of the common and phenotype-specific interactions for the reconstructed networks in each case can be found in Supplementary Table S5.

Systemic lupus (B cells): We used our approach for predicting drug candidates to revert the phenotype of systemic lupus in B cells (GEO: GSE4588). After reconstructing the disease and healthy specific GRNs, the differential network analysis for identifying network stability determinants rendered 11 candidate genes including STAT1 (signal transducer and activator of transcription 1), whose upregulation is associated with onset and progression of systemic lupus.49 The top-ranking drugs were found to be tetrachlorodibenzodioxin (TCDD) (8 targets), cyclosporine (5 targets) and resveratrol (5 targets). Notably, all identified candidate drugs perturb STAT1, indicating their prospective efficacy for treating systemic lupus. Enrichment analysis revealed that cyclosporine and TCDD share a similar enrichment pattern (Figure 3a). However, the enrichment of resveratrol shows a more pronounced effect reflected by higher scores in Figure 3a, and lower AUC of the enrichment cumulative distribution function (CDF) (Table 4). In Supplementary Table S2, we show the analysis of the network response upon drug application and the gene enrichment in multitarget combinations. The simulation assays suggest that resveratrol and TCDD induce a change in the gene expression program of 59.4% and 68.8%, respectively. Thus, application of these drugs constitutes interesting therapeutic formulations for treating systemic lupus in B cells. There exist experimental evidence supporting our predictions, as resveratrol has been found to act as an antiatherogenic agent in human macrophages.50 Also, a positive effect of TCDD on the pathological process of systemic lupus is suggested owing to its immunosuppressive effects in murine systemic lupus.51 Furthermore, cyclosporine was found to represent a helpful treatment of systemic lupus in clinical trials.52 Thus, our analysis reveals cyclosporine, an already known effective treatment for systemic lupus, as well as predicts resveratrol and TCDD as prospective therapeutic interventions.

Rheumatoid arthritis (B cells): In this example, we predicted drug candidates for rheumatoid arthritis in B cells (GEO: GSE4588) using our methodology. We identified 27 candidate genes for perturbation, including a TCF7L2 (transcription factor 7-like 2 (T-cell specific, HMG-box)) polymorphism assumed to be associated to rheumatoid arthritis53 and CDKN1A (cyclin-dependent kinase inhibitor 1A (P21, Cip1)), whose decreased expression has been linked to an increased risk to develop autoimmune diseases, such as rheumatoid arthritis.54 The drugs having more gene targets in the disease network are benzo(a)pyrene (14 targets), copper sulfate (12 targets), TCDD (12 targets), valproic acid (12 targets) and cyclosporine (10 targets). Simulation assays of multitarget combinations show that both TCF7L2 and CDKN1A are included in all combinations inducing the most significant phenotypic change. Enrichment analysis reveals copper sulfate to have the highest enrichment in the top-ranking multitarget combinations, followed by benzo(a)pyrene, TCDD and cyclosporine (Figure 3b and Table 3) underlined by the lower AUC of copper sulfate showing its more specific enrichment in the best multitarget combinations. Simulation assays reveal that copper sulfate reverts 53% of the disease phenotype, whereas cyclosporine only reverts 34% (Supplementary Table S3). Indeed, most of the genes in the core of the disease network are targeted by copper sulfate, explaining its pronounced effect on the gene expression program. In contrast, application of benzo(a)pyrene results in an unstable behavior of the network and is therefore not be considered to cause the phenotypic transition in this disease. Previous studies support these conclusions, showing the beneficial effects of cyclosporine in the short-term treatment of rheumatoid arthritis,55 whereas copper sulfate constitutes a novel approach whose effect on this disease needs to be further elucidated.56

Systemic lupus (CD4 cells): As a last example, we predicted candidate genes and drugs for treating systemic lupus in CD4 cells, starting from the same gene expression data set used in the first example (GEO: GSE4588). We identified 35 candidate genes for perturbation, including STAT1 and other genes relevant to disease pathology, such as IRF7 (interferon
Figure 3  Enrichment of predicted drugs in disease-control examples. Violin plots of drug target enrichment in the space of induced normalized gene expression changes on the basis of simulated multitarget combinations. The white dots represent the mean gene expression change underlined by the variance of the distribution (black bar). The dashed lines represent the maximum enrichment (in percent) of the drugs. The enrichment patterns are contrasted with the corresponding core disease network highlighting drug targets of most enriched drug. (a) Enrichment patterns of drugs having the most targets in the disease network of systemic lupus in B cells reveal resveratrol to be the top-ranking drug. Its drug targets (green) are covering wide ranges of common circuits and perturb STAT1, a hub gene in the network. (b) Enrichment patterns of predicted drugs for rheumatoid arthritis in B cells reveal cyclosporine, copper sulfate and benzoapyrene to have similar enrichment patterns having the highest enrichment in the highest gene expression changes. Cyclosporine and copper sulfate are therefore found to be specific to significantly change the gene expression program from the disease to the healthy phenotype. The pronounced effect of copper sulfate is underlined by its targets in the core of the disease network (green) as it perturbs almost all genes. (c) In case of systemic lupus in CD4+ cells, estradiol and TCDD show the highest enrichments of all candidate drugs. Targets of estradiol (green) are perturbing hub genes of the network, like CDK1, and cover most of the existing circuits of the network.
regulatory factor 7)\(^7\) and ISG15 (ISG15 ubiquitin-like modifier).\(^5\) We identified four drugs targeting the predicted candidate genes, including TCDD (15 targets), acetaminophen (12 targets), estradiol (15 targets) and valproic acid (11 targets). The enrichment analysis of multitarget drug combinations shows that estradiol and TCDD are highly enriched in the predicted candidate genes (Figure 3c), which is further underlined by the AUC value as a deviation of >20% from the uniform AUC proves its higher enrichment in the top-ranking multitarget combinations (Table 4). Simulation assays show that TCDD and estradiol are able to revert 72% and 62% of the disease gene expression program, respectively (Supplementary Table S4), which makes them suitable drugs to treat this disease. As stated previously, TCDD acts as an immunosuppressor in murine systemic lupus,\(^51\) and recent experimental results show the protective effects of estradiol against lupus-mediated hypertension and proteinuria in adult female mice,\(^69\) giving support to our predictions in this case.

**Discussion**

In this work, we propose a method for predicting disease–gene–drug relationships based on the reconstruction of phenotype-specific GRNs underlying phenotypic differences between disease and healthy states, solely relying on differential gene expression data. By following this rationale, we are able to generate more realistic network models to study disease mechanisms by analyzing differences in gene regulatory interactions underlying different cellular states.\(^41,42\) We benchmarked our method for assessing its reliability for differential network inference and showed that our method generates fairly reliable context-specific networks, which are highly enriched in ChIP-Seq validated interactions contained in ENCODE\(^60\) (see Supplementary Table S1.2). We also performed a thorough comparison of our method with two available methods for modeling direct and signed GRNs, namely CellNOptR\(^46\) and SignetTrainer.\(^47\) The results from this comparison (Supplementary Table S2.1 in Supplementary File S2) demonstrate that the GRN models built with our method are more reliable and enriched in experimentally validated interactions than the models generated by other similar methods. After reconstructing phenotype-specific GRNs, we performed a differential network analysis for identifying network motifs determining the stability of disease and healthy phenotypes. In this regard, combinations of positive and negative circuits have been shown to have an important role in the stability of GRNs.\(^21,6\) To derive candidate genes for perturbation, our method first selects optimal combinations of genes belonging to these common circuits between healthy and disease GRNs. Perturbation of these genes should be able to trigger the disease to healthy state phenotypic transition. Second, our method also selects genes under differential regulation – that is, genes regulated by different sets of transcription factors – not belonging to common circuits, as they can only be perturbed individually.

We validated the performance of our methodology for inferring disease–drug relationships by analyzing six data sets of known drug-induced phenotypical changes obtained from the CMap.\(^31\) Our results show that by using our differential network approach, we are able to accurately predict genes and drugs associated with the phenotypic changes, as in most cases the top-ranking solutions are highly enriched in drug gene targets causing the reversion of the disease phenotype \textit{in vitro}.\(^31\) In all validation examples, perturbations of candidate genes in the GRN models cause a change in the global gene expression between healthy and disease states ranging from 42 to 80%. The only exception is the genistein case, in which the number of genes in the reconstructed network model targeted by chemical compounds in databases is rather low.\(^48\) These results highlight that differential topological analyses of GRN models recapitulate phenotypic differences between healthy and disease states, and can be successfully used for identifying genes whose perturbations can induce disease reversion. Thus, unlike current approaches relying on single network topologies, our method is based on a more realistic framework that allows us to more accurately predict genes whose perturbations have a desired phenotypic change, and therefore improving strategies in network pharmacology.\(^9\) In addition, we applied our methodology to three disease-control case studies, for which there is differential gene expression data, to

**Table 4 Statistical comparison of simulated drugs in systemic lupus and rheumatoid arthritis**

| Case                     | Drug                  | AUC   | Difference from AUC of uniform distribution |
|--------------------------|-----------------------|-------|-------------------------------------------|
| Systemic lupus (B cells) | Cyclosporine          | 11.722| 13.17%                                    |
|                          | Resveratrol           | 8.918 | 33.94%                                    |
|                          | Tetrachlorodibenzoxydioxin | 11.61 | 14.00%                                    |
| Systemic lupus (CD4 cells) | Acetaminophen        | 18.721| 12.93%                                    |
|                          | Estradiol             | 16.627| 22.66%                                    |
|                          | Tetrachlorodibenzoxydioxin | 17.111| 20.41%                                    |
|                          | Valproic acid         | 18.615| 13.42%                                    |
| Rheumatoid arthritis (B cells) | Benzo(a)pyrene   | 11.892| 15.05%                                    |
|                          | Copper sulfate        | 11.578| 17.30%                                    |
|                          | Cyclosporine          | 12.169| 13.08%                                    |
|                          | Tetrachlorodibenzoxydioxin | 12.084| 13.69%                                    |
|                          | Valproic acid         | 12.695| 9.32%                                     |

For systemic lupus in B and CD4 cells and rheumatoid arthritis in B cells, the area under the curve (AUC) of the cumulative enrichment distribution function is shown and compared against the AUC of a uniform distribution. Lower AUC values and higher difference from the uniform distribution indicate an enrichment of drug targets in multitarget combinations able to induce a higher change of the gene expression program. The most enriched drugs are highlighted in each case (bold) and agree with the experimentally induced drug.
predict disease–gene–drug relationships constituting prospective clinical treatments being subject to future validations.

Previous approaches aiming at identifying drug perturbations for reverting the disease phenotype solely relied on gene signatures inferred from differential gene expression,\textsuperscript{29,45} or regulatory modules targeted by drugs,\textsuperscript{62,63} without considering gene interactions underlying disease and healthy states. However, the regulatory mechanisms underlying disease pathologies could provide important mechanistic insights on cellular responses to drug application,\textsuperscript{64} and interactions among genes targeted by the drugs in GRNs. Thus, our proposed differential network analysis approach overcomes this drawback by \textit{in silico} simulating network response upon drug application of genes in GRN stability determinants. Indeed, drugs predicted with our approach for reverting the disease-related expression patterns have been validated in experimental studies. In all cases, the three candidate drugs identified to have the most pronounced effects on reverting disease gene expression programs have been used for treating the pathological process of systemic lupus and rheumatoid arthritis. In particular, cyclosporine has been successfully applied in the process of treating systemic lupus and rheumatoid arthritis.\textsuperscript{52,55} However, we predicted resveratrol as a novel treatment of systemic lupus, whose potential therapeutic utility is underlined by previous studies.\textsuperscript{50} Based on these evidences, we are not only able to predict suitable drugs to revert disease-related gene expression patterns but also to significantly narrow down the set of candidate drugs by means of a differential network analysis.

The differential network-based approach to identify disease–gene–drug relationships has been validated with predictions in drug-induced phenotypes in six examples. Interestingly, in all the studied examples we predicted multitarget drug combinations inducing more efficient transitions between disease and healthy phenotypes \textit{in silico}. This could constitute a promising application of our network-based approach for predicting multitarget drug formulations for treating human diseases. Moreover, the application of our approach to systemic lupus and rheumatoid arthritis identified well-known drugs already used in current clinical therapies as well as new prospective treatments subject to future clinical trials. Thus, our method offers a helpful tool to identify disease–gene–drug relationships of other pathological processes to guide experimentalists in the discovery of more effective treatments.

Materials and Methods

Compilation of gene–gene interaction maps from literature resources. To obtain the initial gene interaction maps used throughout this study, we first identified the differentially expressed genes between two cellular phenotypes using an independent two-sample test. In these interaction data sets, we only take into account those genes having a P-value lower than and a fold change higher than the defined case-specific cutoffs that are set depending on the number of genes profiled in each case, and the number of replicates for performing the statistical analysis. After defining the sets of differentially expressed genes in each case, we reconstructed gene interaction maps from experimentally validated interactions reported in scientific publications. For this purpose, we use the information contained in MetaCore from Thomson Reuters, a highly curated resource of biomolecular interactions compiled from literature, to retrieve all direct interactions among differentially expressed genes. Notably, interactions whose effect – that is, activation or inhibition – is unknown are also included in the interaction maps for inferring their corresponding mode of action during the following steps of our methodology. Even though we use validated interactions reported from literature throughout this paper, our methodology is designed to be general and can take advantage of interaction maps generated using different approaches, such as gene coexpression analysis.

Reconstruction of phenotype-specific GRNs. The interaction maps compiled from the literature are rather noisy, comprising experimentally validated interactions reported in different cell lines, tissues or organisms, which makes it difficult to identify the gene interactions taking place in the specific phenotype under study. As the attractors of the initial network are not necessarily matching the studied biological conditions – that is, transcriptomic data – it is necessary to perform a contextualization of the literature interaction maps to derive the phenotype-specific GRNs, as previously described in other recent reports.\textsuperscript{21,65} To accomplish this task, our method implements a genetic algorithm (GA) to contextualize two different GRNs, and makes them compatible to the gene expression profiles of two different cellular phenotypes, such as disease and healthy states. Here, a Boolean modeling formalism with synchronous updating scheme\textsuperscript{66} is used to represent the GRNs to capture the steady state behavior of a molecular network.\textsuperscript{21} Network dynamics are captured by the evolution of each node at the same time, defined by an updating rule that depends on the node's incoming regulatory interactions. Throughout this study, we assume a ‘majority rule’ – that is, a gene is expressed (ON) if it has more incoming activating interactions than incoming inhibiting interactions, and not expressed (OFF) otherwise. Following this logic, a gene having as many activators as inhibitors is considered to be not expressed. However, a gene that is not regulated by any other gene constitutes an exception from this rule as it is assumed to be expressed.

As previously mentioned, the initial interaction maps may contain interactions in which the effect of the interaction (activation or inhibition) among genes is unknown – that is, unsigned interactions. During contextualization, a sign for these interactions is inferred that is consistent with both phenotype-specific networks. The GA is comprised of a population of individuals implemented using a binary array containing an interaction map for both phenotype-specific networks and an inferred sign assignment (Figure 4). The presence of an interaction in a network is represented following a Boolean encoding, letting ‘1’ represent its presence and ‘0’ its absence. In the same manner, we encode the signs of interactions, letting ‘1’ represent activation and ‘0’ inhibition. Consequently, the array representing one individual is split into three subarrays (Figure 4). The first subarray (green) represents the network corresponding to the first phenotype (healthy), and the second subarray (blue) represents the network of the second phenotype (disease), whereas the last subarray (yellow) corresponds to the inferred signs. As we start from the same initial interaction map to contextualize against both phenotypes, the inferred signs have to be identical in both networks.

The complete workflow of the network inference algorithm can be described as follows: for each phenotype-specific GRN, the GA generates a new population of individuals – that is, a set of candidate solutions – in each generation, resulting from the following three-step approach (Figure 4):

\begin{enumerate}
\item \textbf{Selection}: The selection step selects two individuals from the whole population using our own implementation of cooperative selection\textsuperscript{65} to preserve diversity in the population while ensuring the selection of the best individuals at least once. Following this strategy, the best individual is selected and its fitness value is updated to the average of the second and third best fitness values. Thus, this procedure ensures the selection of a different individual in the next selection step – the second best individual – preserving diversity among the best solutions while still disregarding the worst solutions in the population.
\item \textbf{Mutation}: The second step probabilistically alters the selected individuals, by pruning or reintroducing interactions of the network. Moreover, inferred signs are also subject to probabilistic mutations resulting in a flip from activation to inhibition or vice versa. The choice of the mutation probability is, like the choice of the selection scheme, crucial for the performance of the GA. A high mutation probability leads to a more representative exploration of the search space. On the other hand, a low mutation probability allows the GA to converge faster towards an attractor state, even though it may be only a local optimum. The mutation parameter is set to 0.01 per subarray for all examples in the study – that is, 1% of the bits are mutated in every subarray. This conservative choice of the mutation probability allows the algorithm to converge faster while a higher exploration of the search space can still be obtained by increasing the user-defined size of the population.
\end{enumerate}
between network attractors and transcriptomic data is assessed for each individual. A score is derived in taking into account network attractors and stability.

Inference of the effect of unsigned interactions. The estimation of the effects of interactions for which there is no experimental evidence in MetaCore is performed dynamically during the contextualization step. Instead of considering only local network properties, such as gene expression of a regulated gene and its regulator, in our method sign prediction takes into account global network properties. Based on network stability – that is, the convergence to a steady state – and the correspondence between the steady state of the GRN and transcriptomic data, a consistent interaction sign assignment is inferred. Note that the sign inference procedure allows more freedom to the GA to identify network topologies best matching the transcriptomic data. During the analysis of unsigned interactions, network consistency with gene expression data can be increased by pruning network interactions, and also by inferring the best combinations of interaction effect throughout the network. As both GRNs are reconstructed from the same initial interaction map, the inference of interaction effect is performed simultaneously for the two context-specific network representations. We assessed our method's ability to not only infer consistent assignments but also biologically validated ones in Supplementary File S3.

Validation of the network inference algorithm. We benchmarked the performance of our algorithm for reconstructing GRNs by building six networks based on the pairwise differential expression of four well-characterized genome-wide gene expression experiments annotated in ENCODE. In particular, these experiments were performed in three cancer cell lines (GM12878, K562 and HepG2) as well as one embryonic stem cell line (H1-hESC). For each of the six differential expression patterns, starting from a literature-derived interaction map using MetaCore, we assessed the enrichment of ChIP-seq experimentally validated interactions before and after contextualization, to evaluate the performance of our method for identifying phenotype-specific interactions. We also performed a benchmarking of our methodology for reconstructing phenotype-specific GRNs, in comparison with other methods available. We gathered 20 interaction data sets, in which the great majority of the interactions have been experimentally validated (ChIP-seq interaction data from ENCODE), and analyzed them with our method, CellNOptR and SignetTrainer for assessing the accuracy of the reconstructed GRNs for explaining the phenotype-specific gene expression patterns, and the enrichment in experimentally validated interactions in the reconstructed GRNs (Supplementary Table S2.1 in Supplementary File S2).
Selection of validation examples for predicting drugs. We selected six examples for the validation of our methodology from the CMap using different small compounds including celastrol+androgen, gedunin+androgen,32 celastrol, cobalt chloride, estradiol and genistein for treating LNCap or MCF7 cell lines. The examples of celastrol/gedunin+androgen were chosen to illustrate that our method is able to cope with combinations of applied drugs while the others are selected from all available data sets in the CMap having at least three replicates for the control and drug-induced phenotype, and distinct pharmacological mechanisms. Estradiol targets the estrogen receptor and genistein belongs to the class of flavonoids and is an agonist of the estrogen receptor. Celastrol is a quinone methide triterpene inhibiting directly kinases IKKα and IKKβ and inactivates CDC37 (cell division cycle 37) and p23 (prostaglandin E synthase 3) proteins and is thus an HSP90 (heat-shock protein 90 kDa) inhibitor.72 In this context, gedunin has been found to have similar effect and acts as an HSP90 inhibitor as well.72 Ultimately, cobalt chloride is lowering NF-κB (nuclear factor of kappa light polypeptide gene enhancer in B cells) DNA-binding activity and results in higher expression levels of IL-6 (interleukin-6) and TGFβ (transforming growth factor-β) in the brain.73

Selection of candidate genes for network perturbation. We implemented the Johnson’s algorithm72 to detect all elementary network circuits in both reconstructed GRNs, including self-loops. An elementary circuit is a path starting from and ending in the same node visiting each intermediate node only once. We then intersect the set of elementary circuits obtained for both phenotype-specific networks, including positive and negative circuits – that is, between circuits with an even number of inhibitions (positive circuits) and an odd number of inhibitions (negative circuits). Positive circuits have been shown to have an important role in maintaining network stability.73,74 On the other hand, negative circuits are a necessary condition for a network to have an attractive cycle.75 However, it has been shown that combinations of positive and negative circuits are able to maintain a stable steady network state.61 Perturbations of positive circuits have been used in previous studies to induce a transition between two different phenotypes modeled using a single network topology for describing the two phenotype-specific attractor states.31 In this representation, any of the genes contained in a circuit is assumed to be a perturbation candidate and a minimal combination is derived. Nevertheless, our approach takes into consideration the differences between the underlying GRN determining cellular phenotypes, and predicts as candidate genes for perturbation of all the genes contained in positive and negative circuits determining network stability. Owing to the topologic differences between phenotype-specific GRNs, network circuits do not cover similar parts of the networks, and it is more difficult to identify the genes triggering a transition between the two cellular states. Hence, our method relies on a differential network topology analysis to identify genes under differential regulation – that is, genes regulated by different sets of transcription factors – as they constitute ideal perturbation targets, which can only be perturbed individually. The sets of regulators are constrained to expressed genes, as genes that are not expressed cannot contribute to the expression of their targets in the network. The accordingly identified genes are not necessarily those genes responsible for disease onset but are rather genes able to revert most of the gene expression program upon perturbation, which makes them good candidates for pharmacological targeting.

Identification of drugs and multitarget combinations for reverting the disease phenotype. Once the set of candidate genes for perturbation are identified, we simulate multitarget combinations of up to ten candidate genes. Usually, we are interested in a minimal multitarget combination leading to a significant change in the gene expression program between the two cellular phenotypes, which was set to a change of at least 50% of the genes in the GRNs. The size of a multitarget combination is defined as the number of genes contained in it. For each multitarget combination size between 1 and 10 we simulate network response of up to one million combinations and rank the results according to the number of genes whose gene expression is reversed between the two phenotypes. The results are normalized by subtracting the number of perturbed genes from the number of genes whose gene expression is changed upon perturbation. We refer to this normalized gene expression changes in this paper as the multitarget combination score. For relating the determined candidate genes to drugs, we use two different approaches. The first approach, which is used during the validation of our methodology, solely relies on the differential gene expression pattern between the two conditions under study. The differential expression is used as an input for the CMap31 to obtain drugs showing a similar differential expression pattern. We select the top-ranking drugs and determine their target genes by using the Comparative Toxicogenomics Database.48 Later, we compute the enrichment of drug targets in the simulated multitarget combinations. In this approach, each gene is assigned a different weight according to its simulated single perturbation effect, and we analyze the enrichment of the gene targets for the compounds causing the phenotypic transition according to the CMap,31 in the top-ranking multitarget combinations obtained with our method. In addition, network response to induction of a single drug is measured and the drugs are ranked in accordance to the enrichment and this simulation assay analysis. In these simulation assays, the effect of chemical compounds is assumed to be constant during the trial, and the expression values of perturbed genes are kept constant throughout the whole simulation – that is, the drugs are assumed to have dominant effect on the target genes. The second approach solely relies on the Comparative Toxicogenomics Database48 and is used for the prediction of disease-gene–drug relationships in systemic lupus and rheumatoid arthritis. Our method predicts drugs that could have an effect on triggering the phenotypic transition by first identifying the genes in network stability determinants as described above. Then, we identified gene–drug associations by compiling drug mode of action from the Comparative Toxicogenomics Database.34 We then select those drugs having more gene targets among the candidate genes and perform enrichment and simulation assay analysis as described in the previous case.

Analysis of drug–gene target enrichment. To score the drugs obtained from our differential network analysis, we compute the enrichment of drug–gene targets in the set of simulated multitarget combinations. Owing to incomplete information about drug–gene mode of action, not all drug gene targets are represented in our network. Hence, the predicted candidate genes, and therefore the multitarget combinations, do not contain all the drug–gene targets in most cases. Our analysis is therefore restricted to target genes already predicted as perturbation candidates. To study the extent of phenotypic change upon GRN drug perturbation, a weight $w_d$ is assigned to each perturbation candidate, corresponding to the normalized gene expression changes resulting from single-target perturbation of that gene. Then, for each simulated multitarget combination $i$, an enrichment score $m^i$ is derived by summing the weights $w_d$ of targets of drug $d$ contained in the multitarget combination – that is, $m^i = \sum_j w_{d_j}$. To obtain values between 0 and 1, these scores are normalized to obtain $m^i = m^i / \sum_j w^j$. From the values obtained for each multitarget combination, a distribution is drawn over the space of normalized gene expression changes. It is determined by the probability mass function $P_d(x) = s_d(x) / \sum_j s_d(y)$, where $s_d(x) = \sum_i (g_{d_i}(x) - M_d^j)$ and $gec(j)$ is the normalized gene expression change of multitarget combination $j$. To assess finally the quality of a drug with respect to its effect on the phenotype, we derive the cumulative distribution function (CDF) of the scores for each drug and calculate the AUC. Hence, the CDF of enrichment of drug $d$ can be formulated as the step function $c_d(x) = \frac{\max(k;2k-x)}{\min(x;2k-x)} P_d(x)$ and the area under the curve is determined as $AUC_d = \frac{\min(x;2k-x)}{k-\min(x;2k-x)} c_d(x)$. Following the definition of $c_d$ as a monotonously increasing function, an optimal enrichment pattern is reflected by $AUC_d = 0$. Furthermore, smaller values of $AUC_d$ reflect a more favorable drug enrichment pattern as they indicate a lower enrichment in the worst multitarget combinations and at the same time a higher enrichment in the high-ranking combinations.

Conflict of Interest
The authors declare no conflict of interest.

Acknowledgements. This work was supported by the Fond National de la Recherche Luxembourg (grant number C13/BM/5810227). Funding for open access charge: Fond National de la Recherche Luxembourg (grant number C13/BM/5810227).

1. Takahashi K, Yamanaka S. Induction of pluripotent stem cells from mouse embryonic and adult fibroblast cultures by defined factors. Cell 2006; 126: 663–676.
2. Yu J, Vodyanik Ma, Smuga-Otto K, Antosiewicz-Bourget J, Frane JL, Tian S et al. Induced pluripotent stem cell lines derived from human somatic cells. Science2007; 318: 1917–1920.
3. Tiscornia G, Vivas EL, Belmonte JCI. Diseases in a dish: modeling human genetic disorders using induced pluripotent cells. Nat Med 2011; 17: 1570–1576.
4. McLendon R, Friedman A, Bigner D, Van Meir EG, Brat DJ, Mastrogianakis M et al. Comprehensive genomic characterization defines human glioblastoma genes and core pathways. Nature 2008; 455: 1061–1068.
5. Samani NJ, Erdmann J, Hall AS, Hengstlingerg C, Mangho M, Mayer B et al. Genome-wide association analysis of coronary artery disease. N Engl J Med 2007; 357: 443–453.
6. Welcome Trust Case Control C. Genome-wide association study of 14 900 cases of seven common diseases and 3000 shared controls. Nature 2007; 447: 661–678.
7. Hopkins AL. Network pharmacology: the next paradigm in drug discovery. Nat Chem Biol 2008; 4: 682–690.
8. Sonnel AW, Blaincey A, Boldon H, Warrington B. Diagnosing the decline in pharmacological R&F efficiency. Nat Rev Drug Discov 2012; 11: 191–201.
9. Schadt EE, Friend SH, Shwartz DA. A network view of disease and compound screening. Nat Rev Drug Discov 2009; 8: 286–295.
10. Jonsson PF, Bates RA. Global topological features of cancer proteins in the human transcription-factor cross-repression. Stem Cells 2006; 24: 2290–2315.
11. Wanga S, Yonekades W, Wu R. Intersysteme-transcription analysis reveals the high centrality of genes differentially expressed in lung cancer tissues. Bioinformatics 2005; 21: 4026–4028.
12. Goh KI, Cusick ME, Valle D, Childs B, Vidal M, Barabasi AL. The human disease network. Proc Natl Acad Sci USA 2007; 104: 8665–8670.
13. Stassen J. Network medicine: a network-based approach to human disease. Nat Rev Genet 2011; 12: 56–68
14. Franke L, van Bakel H, Folkerts L, de Jong ED, Egmont-Petersen M, Wijmenga C. Reconstruction of a functional human gene network, with an application for prioritizing positional candidate genes. Am J Hum Genet 2008; 7: 1011–1025.
15. Lao K, Karbovig T, Storgard SA, Olsen PI, Pedersen AG, Regina O et al. A human phenome-interactome network of protein complexes implicated in genetic disorders. Nat Biotechnol 2007; 25: 309–316.
16. Calvano SE, Xiao W, Richards DR, Feliciano RM, Baker HV, Cho RJ et al. A network-based analysis of systemic inflammation in humans. Nature 2005; 437: 1032–1037.
17. Lim J, Hao T, Shaw C, Patel AJ, Szabo G, Rual JF et al. A protein–protein interaction network for human inherited ataxias and disorders of purkinje cell degeneration. Cell 2006; 125: 801–814.
18. Pujana MA, Han JD, Stetla LM, Stevens KN, Tewari M, Amin JS et al. Network modeling links breast cancer susceptibility and centrosome dysfunction. Nat Genet 2007; 39: 1338–1343.
19. Zhou JX, Huang S. Understanding gene circuits at cell-fate branch points for rational cell reprogramming. Trends Genet 2011; 27: 55–62.
20. Del Sol A, Crespo I. A general strategy for cellular reprogramming: the importance of transcription factor cross-repression. Semin Cell Dev Biol 2013; 24: 3127–3135.
21. Crespo I, Perumal TM, Jurkowski W, del Sol A. Detecting cellular reprogramming determinants by differential stability analysis of gene regulatory networks. BMC Syst Biol 2013; 7: 140.
22. Del Sol A, Buckley NJ. Concise review: a population shift view of cellular reprogramming. STEM CELLS 2014; 32: 1367–1372.
23. del Sol A, Balling R, Hood L, Galas D. Diseases as network perturbations. Semin Cell Dev Biol 2013; 24: 3127–3135.
24. Crespo I, Krishna A, Le Béchec A, Del Sol A. Predicting missing expression values in gene regulatory networks. J Neurosci Methods 2014; 239: 316–326.
25. Wang Y, Xiao J, Suzek TO, Zhang J, Wang J, Bryant SH. PubChem: a public information resource for chemical structure informatics. Nat Biotechnol 2004; 22: 1413–1416.
26. Law V, Knox C, Djoumbou Y, Jewison T, Guo AC, Liu Y et al. ChemBank: a small-molecule screening and cheminformatics resource database. Nucleic Acids Res 2012; 40: D1032–D1038.
27. Lim J, Hao T, Shaw C, Patel AJ, Szabo G, Rual JF et al. A protein–protein interaction network for human inherited ataxias and disorders of purkinje cell degeneration. Cell 2006; 125: 801–814.
28. Pujana MA, Han JD, Stetla LM, Stevens KN, Tewari M, Amin JS et al. Network modeling links breast cancer susceptibility and centrosome dysfunction. Nat Genet 2007; 39: 1338–1343.
29. Zhou JX, Huang S. Understanding gene circuits at cell-fate branch points for rational cell reprogramming. Trends Genet 2011; 27: 55–62.
30. Del Sol A, Crespo I. A general strategy for cellular reprogramming: the importance of transcription factor cross-repression. Semin Cell Dev Biol 2013; 24: 3127–3135.
31. Crespo I, Perumal TM, Jurkowski W, del Sol A. Detecting cellular reprogramming determinants by differential stability analysis of gene regulatory networks. BMC Syst Biol 2013; 7: 140.
32. Del Sol A, Buckley NJ. Concise review: a population shift view of cellular reprogramming. STEM CELLS 2014; 32: 1367–1372.
33. del Sol A, Balling R, Hood L, Galas D. Diseases as network perturbations. Semin Cell Dev Biol 2013; 24: 3127–3135.
34. Crespo I, Krishna A, Le Béchec A, Del Sol A. Predicting missing expression values in gene regulatory networks. J Neurosci Methods 2014; 239: 316–326.
66. Garg A, D’Carn A, Xenarios I, Mendoza L, De Micheli G. Synchronous versus asynchronous modeling of gene regulatory networks. *Bioinformatics* 2008; 24: 1917–1925.
67. Nepomuceno N, Pinheiro P, Coelho A. *Evolutionary Computation in Combinatorial Optimization*. Springer: Berlin, Heidelberg, Germany, 2007.
68. Durillo JJ, Nebro AJ. *JMetal*: a Java framework for multi-objective optimization. Adv Eng Softw 2011; 42: 769–771.
69. Deb K, Pratap A, Agarwal S, Meyarivan T. A fast and elitist multiobjective genetic algorithm: NSGA-II. *IEEE Trans Evol Comput* 2002; 6: 182–197.
70. Saiminen A, Lehtonen M, Paimela T, Kaarniranta K. Celastrol: molecular targets of Thunder God Vine. *Biochem Biophys Res Commun* 2010; 394: 439–442.
71. Kalpana S, Dhananjay S, Anju B, Lilly G, Sai Ram M. Cobalt chloride attenuates hypobaric hypoxia induced vascular leakage in rat brain: molecular mechanisms of action of cobalt chloride. *Toxicol Appl Pharmacol* 2008; 231: 354–363.
72. Johnson DB. Finding all the elementary circuits of a directed graph. *SIAM J Comput* 1975; 4: 77–84.
73. Plahte E, Mestl T, Omholt SW. Feedback loops, stability and multistationarity in dynamical systems. *J Biol Syst* 1995; 3: 409–413.
74. Snoussi EH. Necessary conditions for multistationarity and stable periodicity. *J Biol Syst* 1998; 6: 3–9.
75. Gouzé J-L. Positive and negative circuits in dynamical systems. *J Biol Syst* 1998; 6: 11–15.
76. Soule C. Graphic Requirements for Multistationarity. *Complexus* 2003; 1: 123–133.
77. Thomas R. The role of feedback circuits: positive feedback circuits are a necessary condition for positive real eigenvalues of the Jacobian matrix. *Berichte der Bunsengesellschaft für physikalische Chemie* 1994; 98: 1148–1151.
78. Thomas R. On the relation between the logical structure of systems and their ability to generate multiple steady states or sustained oscillations. In: Della Dora J, Demongeot J, Lacolle B (eds). *Numerical Methods in the Study of Critical Phenomena*. Springer: Berlin Heidelberg, Germany, 1981, pp 180–193.