Electron attraction mediated by Coulomb repulsion

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One of the defining properties of electrons is their mutual Coulomb repulsion. However, in solids this basic property may change; for example, in superconductors, the coupling of electrons to lattice vibrations makes the electrons attract one another, leading to the formation of bound pairs. Fifty years ago it was proposed† that electrons can be made attractive even when all of the degrees of freedom in the solid are electronic, by exploiting their repulsion from other electrons. This attraction mechanism, termed ‘excitonic’, promised to achieve stronger and more exotic superconductivity. Yet, despite an extensive search, no experimental evidence for excitonic attraction has yet been found. Here we demonstrate this attraction by constructing, from the bottom up, the fundamental building block of the excitonic mechanism. Our experiments are based on quantum devices made from pristine carbon nanotubes, combined with cryogenic precision manipulation. Using this platform, we demonstrate that two electrons can be made to attract each other using an independent electronic system as the ‘glue’ that mediates attraction. Owing to its tunability, our system offers insights into the underlying physics, such as the dependence of the emergent attraction on the underlying repulsion, and the origin of the pairing energy. We also demonstrate transport signatures of excitonic pairing. This experimental demonstration of excitonic pairing paves the way for the design of exotic states of matter.

Following the development of the Bardeen–Cooper–Schrieffer (BCS) theory of superconductivity, W. A. Little proposed the idea that two electrons can attract each other not via phononic-based attraction, but via their repulsion from other electrons. He predicted that if electrons, which are much lighter than ions, mediate the attraction, then the electron pairing would be much stronger than in conventional superconductors. To test this new form of attraction, Little proposed a one-dimensional conducting organic chain (Fig. 1a, green) that has an array of polarizable sidechains (‘polarizers’, purple). Each polarizer has a single electron that can hop between two sites—one closer to and one further away from the main chain. Owing to Coulomb repulsion, an electron travelling down the main chain polarizes the side chains, which in turn attract another electron in the main chain. This mechanism rapidly became popular in attempts to engineer unconventional superconductivity; it was extended to two dimensions, and used in early attempts to explain high-temperature superconductivity. It is a candidate for the unusual superconductivity observed in SrTiO₃ interfaces, and has analogues in optical systems. Numerous attempts have been made to directly synthesize organic materials that have the essential microscopic components; however, so far there has not been any experimental evidence for an excitonic attraction between electrons.

The core of Little’s proposal is the idea that electrons separate into two groups: some form the ‘system’ (Fig. 1a, green), where their mutual interaction is to become attractive, while others make up the surrounding ‘medium’ (purple) that produces the ‘glue’ for the attraction. To make electrons attractive, this medium should perform the unusual feat of flipping the sign of the potential generated by the system electrons, making them look like holes to other system electrons (Fig. 1b). This suggests that the medium should effectively have a negative dielectric constant. Little suggested that this property can be achieved in the dynamic (retarded) limit, in which the system electrons respond faster than the medium, thus leaving a positive polarization cloud in their wake that creates an exponentially weak BCS-like pairing. However, Hirsch and Scalapino showed‡ that the interesting regime of Little’s model is instead the static (instantaneous) limit. Only in that limit does superconductivity dominate over competing orders (such as charge and spin density waves) and the superconducting phase exhibit strong Bose–Einstein-condensation-like pairing.

Here we demonstrate that excitonic pairing is indeed possible and that the key ingredient is the discreteness of the electrons in the medium. We take a bottom-up approach and construct the minimal building block of Little’s model that features excitonic attraction—a two-site system and a single polarizer (Fig. 1a, dashed circle) and show that when the polarizer interacts strongly with the system, it can render its electrons attractive.

The system and polarizer are created within two separate carbon nanotubes, each on its own microchip. We use our recently developed nano-assembly technique to suspend each nanotube between two metallic contacts and above an array of gates (Supplementary Information section S1). In both devices we bias the gates to produce a double-well electrostatic potential along the nanotube length (Fig. 1c). In the polarizer device, the energy levels in the two wells are placed far from the chemical potential in the leads, but close to each other, such that a single electron can hop between the wells, but cannot escape to the leads. The polarizer thus operates as an isolated dipole whose sole degree of freedom is the polarization of its electron (Supplementary Information section S2). Conversely, in the system device, a large central barrier inhibits tunnelling between the two wells, but small side barriers allow electrons to enter from their corresponding leads. On a separately contacted side segment of the system nanotube, we create an independent quantum dot that serves as a charge detector, detecting the population of individual system electrons via weak electrostatic coupling. We then mount the two chips, oppositely facing and perpendicular to each other, in a custom-built scanning probe microscope inside a dilution refrigerator (Fig. 1d). The microscope allows us to control the distance and the coupling between the polarizer nanotube and the system nanotube (Fig. 1d inset) and, hence, to test whether the polarizer alters the behaviour of the system electrons in a fundamental way.

We first measure the charge stability diagram of the bare system, without the polarizer. Using the left and right gates of the system, we scan the potential detuning between the two wells, ∆V = (V₁ − V₂)/2, and their mean potential, V = (V₁ + V₂)/2. Changes in the electronic occupation of the system appear as steps in the charge-detector current, ICD (Supplementary Information section S2). This measurement (Fig. 2a) yields the well-known charge stability diagram of a double
quantum dot with repulsive electrons (explained in Supplementary Information section S3). Tilted charging lines reflect the addition of a single electron to the right or left dot. Near their crossing, the charging lines exhibit a vertical shift (Fig. 2a, dashed black line), reflecting the fact that if one dot is occupied the energy to populate the other dot is increased by the Coulomb repulsion between the neighbouring electrons. This vertical shift is thus a direct fingerprint of the nearest-neighbour attraction. In a bare electronic system, a repulsive Coulomb potential (green) exists at the center of the horizontal vertex, where its magnitude is given by the length of this vertex (2Δ after normalization; see Supplementary Information section S4), reaching Δ = 790 μeV ≈ 8 K.

A medium can transform repulsive system electrons to attractive electrons only if it can flip the sign of the electrostatic potential produced by these electrons. The Coulomb potential of a bare electron is positive in its local and neighbouring sites, implying on-site and nearest-neighbour repulsion (Fig. 2c). In a custom-built scanning probe microscope (centre), operating inside a dilution refrigerator, brings the two oppositely facing devices into proximity (about 100–150 nm apart) such that the polarizer nanotube is perpendicular to the system nanotube (right) and such that one of its dots is directly above the system while the other is further away (left), creating a structure that is analogous to that of Little’s molecule.

The key element for a sign-inverting medium is charge discreteness and, more fundamentally, the fact that a single electron does not repel itself. To understand this, compare the screening by a single-electron dipole to that of a metallic object of similar geometry (Fig. 2e). In a small external field, the charge in the metal will polarize slightly to exactly null the internal field. Conversely, in a dipole with small inter-site tunnelling, an entire electron will polarize between the two sites, creating an internal field that is much larger than, and of opposite sign to, the external field. This behaviour is the basis for our basic ‘sign-inverter’. Unlike continuous charge in a metal that experiences its own field and thus minimizes the electrostatic energy by nulling the internal
state is degenerate between the two even states $(0,0)$ and $(1,1)$ (that is, electrons populating the L/R sites (green/white circles label an electron within the system). By analysing the sign inversion microscopically, for the geometry of our system, we describe the polarizer by the Hamiltonian

$$H_{\text{pol}} = \frac{1}{2} \delta \sigma_z + i \delta \chi$$

in which $\delta \sigma_z = \psi_T^\dagger \psi_T - \psi_B^\dagger \psi_B$, $\delta \chi = \psi_T^\dagger \psi_B + \psi_B^\dagger \psi_T$, $\psi_T$ ($\psi_B$) are creation (annihilation) operators of electrons in the two polarizer sites (‘T’ top; ‘B’ bottom), $\delta = \varepsilon_T - \varepsilon_B$ is the energy detuning between these sites, $t$ is the tunnelling amplitude, and we ignored a constant energy offset. The repulsion between system and polarizer electrons leads to a charge–dipole coupling

$$H_{\text{coup}} = \frac{1}{2} U (n_L + n_R)(\hat{I} - \delta \sigma_z)$$

in which $n_L$ and $n_R$ are the populations of the left and right system sites, $U$ is the repulsion between an electron in one of these sites and an electron in the bottom site of the polarizer (assuming negligible interaction with the top site), and $\hat{I} = \psi_T^\dagger \psi_B + \psi_B^\dagger \psi_T$. This coupling dresses an electron entering the system with a dipolar excitation of the polarizer (see text). The key element for sign inversion is charge discreteness: a single-electron dipole (right) and a similarly shaped metal (left) will best screen the potential to zero far away from the electron, but cannot flip its sign. c. The charge detector is far away from the right dot and that when the polarizer is close their mutual capacitance is strongly screened and so the charging lines of this dot are harder to observe. c, In the bare system, an electron populating the L site generates a Coulomb potential (green) that is positive (repulsive) in both the L and R sites. d, Embedding the system in a medium based on continuum electrostatics (purple) can at best screen the potential to zero far away from the electron, but cannot flip its sign. e. The key element for sign inversion is charge discreteness: a single-electron dipole (right) and a similarly shaped metal (left) will screen an external field differently (grey arrows). In the latter the internal field is nulled, whereas in the former it is larger and of opposite sign to the external field (red arrows; over-screening). This behaviour is rooted in the fact that an electron does not repel itself (see text). f. With a nearby polarizer, an electron charging the system gets dressed by the polarization (grey ellipse). The electrostatic potential (green) of the dressed particle will be substantially different to that of the bare electron (calculated in Supplementary Information section S4). Note that all the measurements presented here were done with single holes instead of single electrons, but to avoid unnecessary confusion we presented the physics in the language of electrons.
the different detuning values. Information section S6). The insets show the polarizer potential wells for observed attraction increases linearly with \( \delta \) (more data in Supplementary Information section S6). The insets show the polarizer potential wells for the different detuning values. d, e, Rationalizing this observation using the polarizer than it is repelled by the original electron that triggered the polarization.

A central prediction of the above model is a direct relationship between the emergent attraction and the underlying repulsion. We test this prediction by changing the separation between the nanotubes, which modifies the repulsion between system and polarizer electrons (U) while keeping the repulsion between the system electrons (W) fixed. The measured dependence of 2.A on U (Supplementary Fig. 6) shows a linear dependence with unit slope. This result follows from equations (1)–(3) in the strong coupling limit (Supplementary Information section S4) and is a demonstration that the observed attraction is driven by repulsion.

Because the ability of the polarizer to dress an electron depends on its polarizability, one might expect that the optimal polarizer detuning for creating the strongest pairing would be at zero detuning (\( \delta = 0 \)). At this detuning, the electronic wavefunction of the polarizer is symmetrically split between its top and bottom sites and its polarizability is maximal. However, the measured charge stability diagrams at different detunings (Fig. 3a–c) show that the attractive correction to the bare repulsion is not maximal at \( \delta = 0 \), but rather increases linearly with \( \delta \). This observation captures an important point about the origin of the pair binding energy, which is most easily rationalized by considering a toy model of a multisite chain (Fig. 3d, e); two far-apart electrons on the chain would each be dressed by two adjacent polarizers (Fig. 3d). In contrast, nearest-neighbour electrons share one polarizer and thus gain the polarization energy of one polarizer (Fig. 3e). This energy gain constitutes the pair binding energy, which is exactly equal to \( \delta \), the stored energy in a polarizer. This is indeed what we observe experimentally. The same mechanism of sharing the dressing costs, leading to a pairing energy of magnitude \( \delta \), also holds in our two-site case, as we explain in Supplementary Information section S6.

Beyond the ground-state stability diagram, we also examine whether pairing is reflected in transport, that is, whether electrons enter the system in pairs. In our set-up, we can measure the current through the polarizer and deduce the behaviour of the system via its strong correlations with the polarizer. To simplify the measurement, we open the barrier to one of the polarizer dots to strongly couple it to the lead, making the polarizer effectively a single quantum dot coupled to two leads (Fig. 4a). Now, the polarization is between dot and lead rather than between two dots. Although these two cases are electrostatically quite similar, they are fundamentally very different: whereas the excitonic polarization of an isolated double dot preserves the overall fermion parity of the combined system and polarizer, tunnelling of an electron to a lead in the polarizer does not. Yet, establishing pairing also in the latter configuration opens possibilities to create quantum systems with engineered dissipation, which may help to stabilize one-dimensional superconductivity.

Figure 4b shows the measured polarizer current, \( I_{\text{pol}} \), with source–drain bias \( V_{SD} = -1.3 \text{ mV} \) as a function of its local gate voltage, \( V_B \), exhibiting a standard Coulomb blockade peak when the occupation of the polarizer dot is free to fluctuate. Owing to the strong coupling to the system, the peak position depends strongly on the electronic occupation of the system (Fig. 4b). If we fix \( V_B \) at 241.5 mV (dashed line in Fig. 4b), then the polarizer conducts for the odd system occupations (1, 0) and (0, 1), but is blocked for the even states. The Coulomb peak is pushed well below the Fermi energy for the (0, 0) state and well above it for the (1, 1) state. This behaviour persists throughout the charge stability diagram of the system (Fig. 4c, \( V_{SD} = 100 \mu \text{V} \)), showing finite current (red) for odd states and negligible current (blue) for even states. Notably, the attraction survives even in the dynamic regime with tunnelling rates being a substantial fraction of the repulsion (\( \Gamma_{\text{pol}}/U \approx 0.2, \Gamma_B/U \approx 0.45 \) and \( \Gamma_I/U \approx 0.23 \)), where \( \Gamma_{L,R,\text{pol}} \) are the tunnelling rates to the left and right contacts of the system and to the polarizer contacts, respectively). Although neither the (0, 0) nor the (1, 1) states support single-particle current, we observe a finite current peak along their degeneracy line (indicated by the arrow in Fig. 4c). Theoretical calculations (Fig. 4d) reproduce this peak only when including correlated many-body events in which an electron hopping in and out of the polarizer is accompanied by a pair of electrons simultaneously co-tunnelling out of and into the system (Supplementary Information section S7).

To better understand the processes underlying the observed current peak, we measure the current along a cut perpendicular to the degeneracy line, as a function of \( \alpha V \) (where \( \alpha \), the independently measured lever-arm, normalizes V to energy units) and for varying \( V_{SD} \) (Fig. 4e). In different bias ranges we observe conductance regimes that differ in their turn-on slope, \( s = dV_{SD}/d(\alpha V) \), which reflects the number of system electrons participating coherently in the dominant conductance regime.
process \((s = 0, 1 \text{ and } 2)\) corresponds to processes with zero, one and two system electrons, respectively. At high bias, \(V_{SD} > 925 \mu \text{eV} \approx U\), we observe \(s \approx 0\) (Fig. 4e, black line), showing that a polarizer electron with enough energy to overcome its interaction with the system electrons \((U)\) can flow without their cooperation. At intermediate bias, \(V_{SD} > 490 \mu \text{eV}\), the observed slope is \(s \approx 1\) (Fig. 4e, blue line), reflecting simultaneous co-tunnelling of one system electron. Below this, and down to zero bias, the slope is \(s \approx 2\) (Fig. 4e, red line), indicating that at low energies a pair of electrons co-tunnels into the system in concert with an electron tunnelling out of the polarizer. Theoretical calculations (Fig. 4f and Supplementary Information section S7) reproduce the main features, although they give a smaller two-electron current than is observed experimentally, probably because they consider these processes to only the lowest order in tunnelling.

Our work experimentally establishes the fundamental concept of excitonic pairing of electrons that was theorized half a century ago. The ability to construct the basic building block of electronic attraction raises many questions regarding the possibility of engineering exotic states of matter by generalizing this concept to larger systems, for example, whether it would be possible to create an artificial superconductor, what kind of pairing such a superconductor would have, and whether it would be stable against competing ground states (see Supplementary Information section S8 for further discussion). The benefit of repulsion-driven attraction is that the pairing energy of the
attraction increases linearly with decreasing device dimensions. Our experiments achieved pairing energies of about 8 K with rather large quantum dots (approximately 400 nm). By extrapolating this value to the nanometre scale, we postulate that it should be possible to reach energies well in excess of room temperature. Given the tremendous progress in engineering quantum dots in two-dimensional semiconductors25–28, down to almost single-atom scale29, the possibilities to engineer interesting states of matter based on electronic attraction now seem very promising.

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