Mean angular diameters, distances and pulsation modes of the classical Cepheids FF Aql and T Vul

CHARA/FLUOR near-infrared interferometric observations

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ABSTRACT

We report the first angular diameter measurements of two classical Cepheids, FF Aql and T Vul, that we have obtained with the FLUOR instrument installed at the CHARA interferometric array. We obtain average limb-darkened angular diameters of \( \theta_D = 0.878 \pm 0.013 \) mas and \( \theta_D = 0.629 \pm 0.013 \) mas, respectively for FF Aql and T Vul. Combining these angular diameters with the HST-FGS trigonometric parallaxes leads to linear radii \( R \approx 33.6 \pm 2.2 R_\odot \) and \( R \approx 35.6 \pm 4.4 R_\odot \), respectively. The comparison with empirical and theoretical Period–Radius relations leads to the conclusion that these Cepheids are pulsating in their fundamental mode. The knowledge of the pulsation mode is of prime importance to determine the Period–Luminosity relation with a uniform sample of fundamental mode Cepheids.

Key words. Techniques: interferometry, high angular resolution ; Stars: variables: Cepheids, distances, oscillations

1. Introduction

The direct detection of angular diameter variations of a pulsating star using optical interferometers has been achieved for many stars now (see e.g. Lane et al. 2002; Kervella et al. 2004; Mérand et al. 2006b; Davis et al. 2009; Lacour et al. 2009). The combination of angular diameters with radial velocity measurements allows us to accurately estimate their distances in a quasi-geometrical way. This independent distance determination is essential to calibrate the Period-Luminosity (P–L) and Period-Radius (P–R) relations of Cepheids. Direct radius measurements also enable us to compare the theoretical (e.g. Neilson et al. 2010) and indirect radius estimates (e.g. Groenewegen 2007).

Having a direct determination of the diameter, we can also settle whether a Cepheid belongs to the fundamental mode group or not, because its average linear diameter should depart from the classical P–R relation. As different modes yield different relations, it is essential to know the pulsation mode in order to calibrate the P–L relation from a homogeneous sample of Cepheids.

We present here the first interferometric observations of the Cepheids FF Aql and T Vul. The former has a small amplitude (less than 0.5 mag in V), a sinusoidal-like light curve, and is therefore generally designated as a s-Cepheid. The s-Cepheids are suspected to be first overtone pulsators (see e.g. Bohm-Vitense 1988). T Vul has the same pulsation period that FF Aql but is expected to pulsate in the fundamental mode. These Cepheids also belong to binary systems with a hotter companion. From IUE spectra, Evans et al. (1991) detected around FF Aql a companion with a spectral type between A9 V and F3 V. This corresponds to a magnitude difference with respect to the Cepheid \( \Delta K \sim 6.1–6.5 \) mag. Evans (1992) found that the companion is a A0.8 V star, also estimated from IUE spectra, and corresponds to a magnitude difference \( \Delta K \sim 5.2 \) mag.

In this paper, we focus on determining the distance and radius of these Cepheids using the interferometric Baade-Wesselink method (IBWM). We also compare the linear radii with those in the literature and with published P–R relations in order to reveal the pulsation mode.

2. Interferometric observations

The observations were performed in June 2010 and August 2011 at the CHARA Array (ten Brummelaar et al. 2005) in the near infrared K' band (1.9 < \( \lambda < 2.3 \mu m \)) with the Fiber Linked Unit for Optical Recombination (FLUOR; Coudé du Foresto et al. 2003, Mérand et al. 2006a). For these observations, we used baselines longer than 200 m in order to resolved sufficiently well the two targets. The journal of the observations is presented in Table 1.

The squared visibility of the fringes has been estimated from the raw data using the FLUOR data reduction software (Coudé du Foresto et al. 1997, Mérand et al. 2006a), based on the integration of the fringes power spectrum. The raw squared visibilities have then been calibrated using resolved calibrator stars, chosen from the catalogue of Mérand et al. (2005a), using criteria defined to minimize the calibration bias and maximize the signal-to-noise ratio. The calibrators used for these observations are listed in Table 1. They were observed immediately before and/or after the Cepheid in order to monitor the interferometric transfer function of the instrument. The error introduced by the uncertainty on each calibrator’s estimated angular diameter has been propagated using the formalism developed by

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Table 1. Calibrated squared visibility measurements of FF Aql.

| Star   | MJD   | φ     | B (m) | PA  (°) | V² ± σ |
|--------|-------|-------|-------|--------|--------|
| FF Aql | 55352.404 | 0.36  | 318.98 | 25.1   | 0.2940 ± 0.0205 |
|        | 55352.433 | 0.36  | 312.70 | 19.3   | 0.3958 ± 0.0244 |
|        | 55353.431 | 0.58  | 273.78 | -44.0  | 0.4774 ± 0.0151 |
|        | 55355.436 | 0.03  | 310.34 | 16.7   | 0.3584 ± 0.0126 |
|        | 55366.374 | 0.48  | 219.94 | 62.9   | 0.6192 ± 0.0175 |
|        | 55779.257 | 0.83  | 314.15 | 20.7   | 0.3839 ± 0.0095 |
|        | 55781.254 | 0.27  | 309.83 | 72.1   | 0.3535 ± 0.0120 |
|        | 55782.317 | 0.51  | 230.92 | 0.1    | 0.5813 ± 0.0159 |
|        | 55784.287 | 0.95  | 278.37 | -48.7  | 0.4678 ± 0.0200 |
|        | 55786.266 | 0.40  | 308.46 | 14.4   | 0.3506 ± 0.0136 |
|        | 55786.290 | 0.40  | 304.97 | 8.7    | 0.3807 ± 0.0144 |
|        | 55790.230 | 0.28  | 249.54 | 76.0   | 0.5141 ± 0.0126 |

Table 2. Calibrators used for the observations.

| Calibrator | m_V | m_K | Spec. Type | θ_UD (mas) | γ (°) |
|-----------|-----|-----|------------|------------|-------|
|            |     |     |            |            |       |
| HD 172169  | 6.7 | 4.1 | K1III      | 0.942 ± 0.012 | 13.1 |
| HD 169113  | 7.1 | 3.9 | K1III      | 0.816 ± 0.011 | 13.3 |
| HD 187193  | 6.0 | 3.9 | K0III-III  | 0.893 ± 0.012 | 14.0 |
| HD 198330  | 7.3 | 3.8 | K4III      | 0.913 ± 0.012 | 2.6  |
| HD 201051  | 6.1 | 4.0 | K0III-III  | 0.827 ± 0.011 | 3.6  |
| HD 192944  | 5.3 | 3.0 | G8III      | 1.085 ± 0.015 | 8.5  |
| HD 187193  | 6.0 | 3.9 | K0III-III  | 0.893 ± 0.012 | 14.5 |

Notes. MJD is the date of the observations (Modified Julian Date), φ the phase of pulsation, B the telescope projected separation, PA the baseline projection angle, and V² the squared visibility.

Notes. m_V, m_K: magnitudes in V and K bands; θ_UD: uniform disk angular diameter in K band; γ: angular distance to the Cepheid.

The final uncertainty of the calibrated squared visibility includes statistical (from the dispersion of the raw squared visibilities obtained during the observations) and systematic errors (from the error bars on the calibrators).

For each night we observed a Cepheid, we determined a uniform disk diameter based on one or several squared visibility measurements (Table 1). Each night was assigned a unique pulsation phase established using the average date of observation and the Samus et al. (2009) ephemeris: P = 4.470916 days and T₀ = 2441576.4280 for FF Aql, and P = 4.435462 days and T₀ = 2441705.1210 for T Vul.

3. The interferometric Baade–Wesselink method

The IBWM makes use of radial velocity and angular diameter measurements of the star during its pulsation cycle. This involves a good phase coverage and the highest possible angular resolution. The integral over time of the radial velocity is then directly linked to the angular diameter variation.

The presence of a companion can falsify the results if its magnitude is close to the one of the Cepheid, and if the orbital effect is detectable in the spectroscopic measurements. In our case, these main sequence companions are faint compared to the Cepheids, and do not affect the photometric signals. Only the radial velocities are affected by the presence of the companions and have to be corrected.

3.1. Radial velocity integrations

Among published radial velocities data of FF Aql, we chose Evans et al. (1990) for two reasons. First, the orbital motion causes by the presence of the companion was already removed from measurements, only leaving the displacement due to the pulsating photosphere. Secondly, the radial velocities were extracted using the cross-correlation method. As shown by Nardetto et al. (2004), the method used can affect the distance determination via the choice of the projection factor (hereafter p-factor), which we will introduce in Sect. 3.2. For T Vul, we use the radial velocities of Bersier et al. (1994), also from the cross-correlation method. The amplitude of the orbital motion was not detected with this data so we did not apply any corrections due to the presence of the companion. For both Cepheids, we re-determined the pulsation phases using the ephemeris presented previously.

The radial velocities, which were acquired at irregular phases, must be numerically integrated to get the radial displacement. The best way to achieve a robust integration and avoid noisy data is to interpolate the data before integration. For this purpose, the radial velocities were smoothly interpolated using a periodic cubic spline function, defined by floating nodes. This method was already used by Mérand et al. (2007), and we refer the reader to this paper for a detailed explanation. The interpolated curves for our two Cepheids are presented in Fig. 1. The dispersion of the residuals are σ = 61 m s⁻¹ and σ = 68 m s⁻¹, respectively for T Vul and FF Aql.

3.2. Distance determination

Our angular diameter measurements were then fitted to the radial displacements to get the distance d:

\[ \theta_{UD}(T) - \theta_{UD}(0) = -\frac{2kp}{d} \int_{0}^{T} (v_r(t) - v_y) dt, \]

where \( p \) is the so-called p-factor, defined as the ratio between the pulsation velocity and the radial velocity (measured by spectroscopy), \( \theta_{UD} \) the interferometric angular diameter for a uniform disk model, \( k \) the ratio between the uniform and the limb-darkened stellar diameter, and \( v_y \) the systemic velocity.

The parameters of the fit are the average angular diameter \( \theta(0) \), the quantity \( d/kp \) and a possible variation in the pulsation period between interferometric and spectroscopic observations.

The p-factor depends on detailed modelling of stellar atmosphere, but such models are only available for a few Cepheids and we conventionally choose a multiplicative constant factor. Nardetto et al. (2004) showed that the choice of a constant factor instead of a time-dependent ones gives a systematic error in the final distance of \( \sim 0.2 \% \), which is below the best relative precision of current distance estimates. Mérand et al. (2005) presented the unique measured value \( p = 1.27 ± 0.06 \) for δ Cep.
Although there is no agreement in the literature on the optimum value of the $p$-factor, it is clear that it depends on each Cepheid. Different authors use either constant $p$-factor values (ranging from 1.27 to 1.5), or a dependence with the pulsation period. The period dependence is likely to reflect the dependence with the limb darkening. For this work, we chose the latest $p$-factor relation $p = 1.550_{-0.034}^{+0.036} - 0.186_{-0.068}^{+0.073} \log P$ of Storm et al. (2011), because this is an empirical relation based on the largest sample of Cepheids, and covering the widest range of periods. We have for both stars $p = 1.43 \pm 0.06$.

The $k$ parameter is generally determined assuming a limb-darkened disk model and is expected to vary with the pulsation phase. However, in the near-IR, Marengo et al. (2003) showed from hydrodynamic models in spherical geometry that $k$ is constant with the pulsation at a level of 0.2%. From hydrostatic models, Mérand (2008) found a variation of $k$ of the order of 0.4%. Our interferometric measurements are not sensitive to this variation and we therefore assumed a constant limb-darkening coefficient. The hydrostatic model computed from Claret coefficients (Claret 2000), with the average stellar parameters $T_{\text{eff}} = 6000 \, \text{K}$, $\log g = 2$, $\text{Fe}/\text{H} = 0.0$ and $V_t = 4 \, \text{km s}^{-1}$ from Luck et al. (2008) for FF Aql and Andrievsky et al. (2005) for T Vul, corresponds to $k = 0.985$. The IBWM fit yields for FF Aql a distance $d = 363 \pm 73 \, \text{pc}$ and an average angular uniform disk diameter $\theta_{\text{UD}} = 0.865 \pm 0.013 \, \text{mas}$, with a total reduced $\chi^2$ of 0.4. For T Vul, we obtain $d = 415 \pm 100 \, \text{pc}$ and $\theta_{\text{UD}} = 0.620 \pm 0.012 \, \text{mas}$, with a total reduced $\chi^2$ of 2.5. These results are summarized in Table 3 and the angular diameter variations are plotted in Fig. 2. We also allowed a change in the period for FF Aql and T Vul of $\sim 14 \, \text{s}$ and $\sim -26 \, \text{s}$, respectively.
3.3. Linear radius

We transformed the uniform disk diameters to limb-darkened disk diameters using the value of $k$ previously chosen, we get $\theta_{\text{UD}} = 0.878 \pm 0.013$ mas for FF Aql and $\theta_{\text{UD}} = 0.629 \pm 0.013$ mas for T Vul. These measured values, which have an accuracy $\sim 1.5\%$, are in good agreement with those predicted from IR surface brightness method (e.g. Moskalik & Gorynya 2005 Groenewegen 2007). The fitted distance of FF Aql is also consistent with the derived value $d = 356 \pm 23$ pc from the HST-FGS parallax of Benedict et al. (2007). The same authors give for T Vul $d = 526 \pm 64$ pc, that is $\sim 27\%$ larger than our value, but within 1.1$\sigma$. As the values from Benedict et al. (2007) are more accurate and do not depend on a $p$-factor assumption (compared to our fitted distances), we preferred them to evaluate the linear radius. We therefore used the HST-FGS distances in the BW fit and obtained $R = 33.6 \pm 2.2 R_\odot$ and $R = 35.6 \pm 4.4 R_\odot$, respectively for FF Aql and T Vul.

In our analysis, we did not take into account a possible circumstellar envelope (CSE) emission, that could lead to an over-estimate of the angular diameter. From the spectral energy distribution of FF Aql given by Gallenne et al. (2011), the infrared excess caused by the CSE appears around 10 $\mu$m, while it is negligible at 2.2 $\mu$m. We assumed this is also the case for T Vul.

3.4. $p$-factor

We can use the HST-FGS distances in Eq. 1 to directly fit the $p$-factor, as already done by Merand et al. (2005) for $\delta$ Cep. We get $p = 1.40 \pm 0.28$ and $p = 1.81 \pm 0.44$, for FF Aql and T Vul respectively. These estimates can be compared with the empirical and theoretical $p$–P relations, respectively from Storm et al. (2011) and Nardetto et al. (2009). For FF Aql, the $p$-factor is compatible with the value derived from the empirical relation, while the estimate of T Vul is within 1$\sigma$. Although at odds with the theoretical relation, our estimates are not accurate enough to constrain it.

A direct determination of the $p$-factor is a powerful constraint to numerical atmosphere models of Cepheids, however our work does not contain enough measurements to have an accurate estimate of this parameter for these stars.

4. Period–Radius relation

The estimated linear radii can be compared with empirical and theoretical Period–Radius ($P$–$R$) relations, that are of the form

$$\log R = a \log P + b.$$ 

We chose the recent theoretical calculations from Neilson et al. (2010), who used a pulsation-driven mass loss model. We also selected the recent works of Groenewegen (2007), who used Cepheids with known distances and angular diameters to derive an empirical $P$–$R$ relation. These two relations are only valid for fundamental mode Cepheids.

In principle, the position of a Cepheid in the $P$–$R$ diagram can reveal its pulsation mode, if the estimated radius is sufficiently accurate. We plotted in Fig. 3 the $P$–$R$ relations (thick curves) and our estimated linear radii. The intrinsic dispersion of each relation is represented with thinner curves (with the same colour and symbol). We notice that both Cepheids are consistent (within the intrinsic dispersion) with stars pulsating in a fundamental mode. We also plotted with triangles the radii assuming an overtone pulsation, using the ratio of the overtone period $P_1$ to the fundamental period $P_0$ given by $P_1/P_0 = 0.720 - 0.027 \log P_0$ (Alcock et al. 1995). In addition, we represented with squares the radii of the star assuming first overtone pulsation, by using the theoretical first overtone $P$–$R$ relation of Bono et al. (2001). The overtone mode seems not compatible with the $P$–$R$ relations, and therefore suggest that FF Aql and T Vul are pulsating in the fundamental mode.

5. Conclusions and discussion

We report the first interferometric observations of two classical Cepheids, FF Aql and T Vul, with the CHARA/FLUOR instrument. The angular diameter variations were monitored over Table 3. Cepheid average angular diameters and distances determined through the application of the interferometric BW method.

| Star   | $\theta_{\text{UD}}$ (mas) | $\theta_{\text{UD}}$ (mas) | $d$ (pc) | $d_{\text{HST}}$ (pc) | $R$ ($R_\odot$) | $\chi^2$ |
|--------|-----------------|-----------------|--------|-----------------|----------------|--------|
| FF Aql | 0.865 ± 0.013   | 0.878 ± 0.013   | 363 ± 73 | 356 ± 23 | 33.6 ± 2.2 | 0.4    |
| T Vul  | 0.620 ± 0.012   | 0.629 ± 0.013   | 415 ± 100 | 526 ± 64 | 35.6 ± 4.4 | 2.5    |

Notes. The linear radius $R$ were estimated using the more accurate distances $d_{\text{HST}}$ derived by Benedict et al. (2007).
the pulsation cycle and combined with previously published radial velocity measurements to get an independent estimate of the distance and mean angular diameter. The precision achieved is \( \sim 2\% \) on their average angular diameter estimates.

We found for FF Aql a good agreement (0.3\sigma) between our fitted distance and the HST-FGS estimate \( \text{Benedict et al. 2007}. \) For T Vul, a discrepancy is found between the two estimates, our value being \( \sim 27\% \) smaller, but within 1.1\sigma. The main source of bias in the use of the BW method is the choice of the \( p \)-factor, and that could explain the discrepancy encountered. We can also note that more interferometric measurements, with higher accuracy, would also reduce this discrepancy. To avoid a possible bias on the distance due to the \( p \)-factor assumption, we coupled our angular diameters with existing trigonometric parallaxes to evaluate the linear radii.

When we compared the linear radii with empirical and theoretical \( P-R \) relations, we showed that these two short period Cepheids are pulsating in their fundamental mode. Our work confirms the pulsation mode of T Vul, already flagged as fundamental pulsator by several authors \( \text{e.g. Groenewegen, 2000, and references therein}. \) However this is not the case for FF Aql. This \( s \)-Cepheid, with small light amplitude and practically sinusoidal light curve, is usually considered as pulsating in the first overtone \( \text{e.g. Sachkov, 1997}. \) As the pulsation mode is generally identified by Fourier decomposition of the light curve or the radial velocity curve, the presence of a companion around FF Aql could lead to an error in the determination of the pulsation mode. If the difference between the magnitude of the Cepheid and that of its companion is small, the apparent magnitude of the Cepheid will be falsified. The radial velocity measurements can also be altered because of the orbital effect.

The knowledge of the pulsation mode is of prime importance to calibrate the \( P-L \) relation with an uniform sample of fundamental mode Cepheids, since different modes will yield different relations.

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References

Alcock, C., Allsman, R. A., Axelrod, T. S., et al. 1995, AJ, 109, 1653
Andrievsky, S. M., Luck, R. E., & Kovtyukh, V. V. 2005, AJ, 130, 1880
Benedict, G. F., McArthur, B. E., Feast, M. W., et al. 2007, AJ, 133, 1810
Bersier, D., Burki, G., Mayor, M., & Duquennoy, A. 1994, A&AS, 108, 25
Bohm-Vitense, E. 1988, ApJ, 324, L27
Bono, G., Caputo, F., & Marconi, M. 2001, MNRAS, 325, 1353
Claret, A. 2000, A&A, 363, 1081
Coudé du Foresto, V., Borde, P. J., Merand, A., et al. 2003, in SPIE Conference Series, ed. W. A. Traub, Vol. 4838, 280–285
Coudé du Foresto, V., Ridgway, S., & Mariotti, J. 1997, A&AS, 121, 379
Davis, J., Jacob, A. P., Robertson, J. G., et al. 2009, MNRAS, 394, 1620
Evans, N. R. 1992, AJ, 104, 216
Evans, N. R., Welch, D. L., Scarfe, C. D., & Teays, T. J. 1990, AJ, 99, 1598
Gallenne, A., Kervella, P., & Merand, A., 2011, A&A, 538, A24
Groenewegen, M. A. T. 2000, A&A, 363, 901
Groenewegen, M. A. T. 2007, A&A, 474, 975
Kervella, P., Nardetto, N., Bersier, D., Mourard, D., & Coudé du Foresto, V. 2004, A&A, 416, 941
Lacour, S., Thibault, E., Perrin, G., et al. 2009, ApJ, 707, 632.
Lané, B. F., Creech-Eakman, M. J., & Nordgren, T. E. 2002, ApJ, 573, 330
Luck, R. E., Andrievsky, S. M., Fokin, A., & Kovtyukh, V. V. 2008, AJ, 136, 98
Marengo, M., Karovska, M., Sasselov, D. D., et al. 2003, ApJ, 589, 968
Merand, A. 2008, in EAS Publications Series, Vol. 28, EAS Publications Series, ed. S. Wolf, F. Allard, & P. See, 53–59
Merand, A., Aufdenberg, J. P., Kervella, P., et al. 2007, ApJ, 664, 1093
Merand, A., Boryé, P., & Coudé Du Foresto, V. 2005a, A&A, 433, 1155
Merand, A., Coudé du Foresto, V., Kellerer, A., et al. 2006a, in SPIE Conference Series, Vol. 6268, 46
Merand, A., Kervella, P., Coudé du Foresto, V., ten Brummelaar, T., & McAlister, H. 2006b, MSAI, 77, 231
Moskalik, P. & Gorynya, N. A. 2005, Acta Astronomica, 55, 247
Nardetto, N., Fokin, A., Mourard, D., et al. 2004, A&A, 428, 131
Nardetto, N., Gieren, W., Kervella, P., et al. 2009, ArXiv e-prints
Neilson, H. R., Ngeow, C., Kanbur, S. M., & Lester, J. B. 2010, ApJ, 716, 1136
Perrin, G. 2003, A&A, 400, 1173
Sachkov, M. E. 1997, Information Bulletin on Variable Stars, 4522, 1
Samus, N. N., Durlevich, O. V., & et al. 2009, VizieR Online Data Catalog: B/gcvs. Originally published in: Institute of Astronomy of Russian Academy of Sciences and Sternberg, State Astronomical Institute of the Moscow State University, 1, 2025
Storm, J., Gieren, W., Fosqué, P., et al. 2011, A&A, 534, A94
ten Brummelaar, T. A., McAlister, H. A., Ridgway, S. T., et al. 2005, ApJ, 628, 453

A. Gallenne et al.: CHARA/FLUOR interferometric observations of FF Aql and T Vul