Gas and dark matter in the Sculptor group: NGC 300

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ABSTRACT

We used the Australia Telescope Compact Array to map a large field of approximately $2^\circ \times 2^\circ$ around the Sculptor group galaxy NGC 300 in the 21-cm line emission of neutral hydrogen. We achieved a $5\sigma$ H$_i$ column density sensitivity of $10^{19}$ cm$^{-2}$ over a spectral channel width of 8 km s$^{-1}$ for emission filling the $180 \times 88$ arcsec$^2$ synthesized beam. The corresponding H$_i$ mass sensitivity is $1.2 \times 10^5$ M$_{\odot}$, assuming a distance of 1.9 Mpc. For the first time, the vast H$_i$ disc of NGC 300 has been mapped over its entire extent at a moderately high spatial resolution of about 1 kpc.

NGC 300 is characterized by a dense inner H$_i$ disc, well aligned with the optical disc of $290^\circ$ orientation angle, and an extended outer H$_i$ disc with a major axis of more than 1$^\circ$ on the sky (equivalent to a diameter of about 35 kpc) and a different orientation angle of $332^\circ$. A significant fraction (about 43 per cent) of the total detected H$_i$ mass of $1.5 \times 10^9$ M$_{\odot}$ resides within the extended outer disc. We fitted a tilted ring model to the velocity field of NGC 300 to derive the rotation curve out to a radius of 18.4 kpc, almost twice the range of previous rotation curve studies. The rotation curve rises to a maximum velocity of almost 100 km s$^{-1}$ and then gently decreases again in the outer disc beyond a radius of about 10 kpc. Mass models fitted to the derived rotation curve yield good fits for Burkert and NFW dark matter halo models, whereas pseudo-isothermal halo models and Modified Newtonian Dynamics (MOND)-based models both struggle to cope with the declining rotation curve.

We also observe significant asymmetries in the outer H$_i$ disc of NGC 300, in particular near the edge of the disc, which are possibly due to ram-pressure stripping of gas by the intergalactic medium (IGM) of the Sculptor group. Our estimates show that ram-pressure stripping can occur under reasonable assumptions on the density of the IGM and the relative velocity of NGC 300. The asymmetries in the gas disc suggest a proper motion of NGC 300 towards the south-east. At the same time, our data exclude IGM densities of significantly higher than $10^{-5}$ cm$^{-3}$ in the vicinity of NGC 300, as otherwise the outer gas disc would have been stripped.

Key words: galaxies: individual: NGC 300 – galaxies: kinematics and dynamics – galaxies: structure – radio lines: galaxies.

1 INTRODUCTION

At distances in the range of about 2 to 5 Mpc, the Sculptor group is among the nearest galaxy groups beyond the Local Group (Jerjen, Freeman & Binggeli 1998). It forms an elongated filament of galaxies and comprises a number of separate subgroups at different distances along the line of sight. At a distance of about 2 Mpc, the nearest of these subgroups consists of NGC 55, NGC 300, and possibly two or more known dwarf spheroidal companions (Karachentsev et al. 2003; Koribalski et al., in preparation). NGC 55 and 300 are medium-sized spiral galaxies of type SB(s)m and SA(s)d, respectively (de Vaucouleurs et al. 1991). Their proximity makes them preferential targets for deep H$_i$ observations with high spatial resolution and H$_i$ mass sensitivity.

Some of the basic properties and physical parameters of NGC 300, including the results of this work, are listed in Table 1. The distance towards NGC 300 has been measured with great accuracy and through different methods. Rizzi et al. (2006) used the tip of the red giant branch to determine distance moduli of $(m - M)_0 = 26.30 \pm 0.03 \pm 0.12$ and $26.36 \pm 0.02 \pm 0.12$ mag through two different statistical methods as part of the Araucaria Project (Gieren et al. 2005b). Their results are consistent with the distance moduli of $26.43 \pm 0.04 \pm 0.05$ and $26.37 \pm 0.05 \pm 0.03$ mag.
Table 1. Properties of NGC 300. The separation between inner and outer H\textsc{i} disc was made at a column density level of 5 \times 10^{20} cm^{-2}. Note that all errors are statistical uncertainties and do not reflect possible systematic errors. References: [1] de Vaucouleurs et al. (1991); [2] Gieren et al. (2005a); [3] Rizzi et al. (2006); [4] Carignan (1985). Values without reference are the result of this study.

| Parameter          | Value | Unit | Ref. |
|--------------------|-------|------|------|
| Type               | SA(s)d|      |      |
| \(a (\text{J2000})\) | 00\text{h}54\text{m}53.4\text{s} |      | [1]  |
| \(b (\text{J2000})\) | -37\text{\deg}41\text{\arcmin}02\text{\arcsec}\ |
| Distance           | 1.9   | Mpc  | [2]  |
| \(R_{25}\)         | 9.8   | arcmin | [3] |
| Radial velocity    |       |      |      |
| Barycentric        | 144 \pm 2 | km s\textsuperscript{-1} |      |
| LSR                | 136 \pm 2 | km s\textsuperscript{-1} |      |
| Position angle\textsuperscript{a} |       |      |      |
| Inner disc         | 290/0 \pm 0.5 |      |      |
| Outer disc         | 331/7 \pm 0.3 |      |      |
| Inclination        | 40\textdegree\ldots50\textdegree |      |      |
| Max. rot. velocity | 98.8 \pm 3.1 | km s\textsuperscript{-1} |      |
| Integrated flux    | 1.72 \times 10\textsuperscript{4} | Jy km s\textsuperscript{-1} |      |
| H\textsc{i} mass   | 1.5 \times 10\textsuperscript{5} | M\odot |      |
| Inner disc         | 8.5 \times 10\textsuperscript{4} | M\odot |      |
| Outer disc         | 6.5 \times 10\textsuperscript{4} | M\odot |      |
| Gas mass\textsuperscript{b} | (1.9 \pm 0.2) \times 10\textsuperscript{5} | M\odot |      |
| Stellar mass\textsuperscript{b} | (1.0 \pm 0.1) \times 10\textsuperscript{5} | M\odot |      |
| Total mass\textsuperscript{b} | (2.9 \pm 0.2) \times 10\textsuperscript{5} | M\odot |      |

\textsuperscript{a}w.r.t. the J2000.0 equatorial coordinate system.

\textsuperscript{b}Across our tilted ring area (0.9 < r < 18.4 kpc).

\textsuperscript{c}Within \(r = 18.4\) kpc.

derived from Cepheid variables by Gieren et al. (2004, 2005a), respectively. Based on these measurements we therefore adopt a distance of 1.9 Mpc for NGC 300 throughout this paper.

Early H\textsc{i} imaging of NGC 300 was carried out by Shobbrook & Robinson (1967) using the 64-m Parkes radio telescope. They determined an H\textsc{i} mass of 2.1 \times 10\textsuperscript{6} M\odot and a total mass of (2.5 \pm 0.5) \times 10\textsuperscript{10} M\odot from the rotation curve under the assumption of a distance of 1.9 Mpc. They also noticed that the velocity field of NGC 300 appears strongly distorted which they attributed to the gravitational influence of a large H\textsc{i} cloud to the south-east of the galaxy. This cloud, however, was later found to be most likely part of the Magellanic Stream (Mathewson, Cleary & Murray 1975; Rogstad et al. 1979). A larger area around NGC 300 was mapped in H\textsc{i} by Mathewson et al. (1975) with the 64-m Parkes radio telescope. Within their brightness temperature sensitivity of 0.3 K over 4.1 km s\textsuperscript{-1} and across the 15 arcmin Parkes beam they detected several extended gas clouds with velocities comparable to those found across NGC 300, including a long ‘H\textsc{i} tail’ extending about 2\textdegree to the southeast of the galaxy. While Mathewson et al. (1975) assumed that these clouds were associated with NGC 300, there has been a long debate over the past decades whether they might instead be fragments of the Magellanic Stream that runs across the same part of the sky (e.g. Haynes & Roberts 1979; Putman et al. 2003). A more detailed H\textsc{i} image of NGC 300 was obtained by Rogstad et al. (1979) with the twin-element interferometer of the Owens Valley Radio Observatory. At a much higher angular resolution of 2 \times 3 arcmin\textsuperscript{2} half-power beam width they were able to derive a detailed radial velocity map of the inner part of the galaxy. By fitting a tilted ring model to the velocity field they were able to describe the distorted velocity contours of NGC 300 as a result of varying inclination and position angle across the H\textsc{i} disc. The rotation curve obtained by Rogstad et al. (1979) from the tilted ring model is basically flat beyond a radius of about 10 arcmin with a turnover velocity of 94 km s\textsuperscript{-1} at 16 arcmin radius. They suggest that the warping of the H\textsc{i} disc of NGC 300 could have been caused by a close encounter with another galaxy or massive H\textsc{i} cloud within the past 10\textsuperscript{9} years. Similar H\textsc{i} synthesis observations of NGC 300 with somewhat higher angular resolution (50 \times 50 arcsec\textsuperscript{2} half-power beam width) were obtained by Puche, Carignan & Bosma (1990) who employed a mosaic of five pointings with the Very Large Array (VLA).

Unfortunately, the synthesis images obtained by Rogstad et al. (1979) and Puche et al. (1990) did not reveal the extent and structure of the outer disc of NGC 300 due to insufficient field of view and lack of sensitivity. We therefore decided to obtain deep H\textsc{i} observations of a large field of 2\textdegree \times 2\textdegree around NGC 300 in a mosaic of 32 pointings with the Australia Telescope Compact Array (ATCA). The aim of these observations was to map the entire extent of the H\textsc{i} disc of NGC 300, determine its structure, and dynamics, and search for extra-planar gas in the vicinity of the galaxy. The observations and results of this project are described in this paper. Similar observations of the Sculptor group galaxy NGC 55 will be presented in a separate paper.

This paper is organized as follows. Section 2 describes our observations and data reduction procedure. In Section 3, we discuss our results, including the general physical parameters of NGC 300 and the results of the rotation curve analysis. In Section 4, we describe the fitting of mass models, with and without dark matter, to the observed rotation curve. In Section 5, we discuss the possible origin of the extended outer gas disc of NGC 300 and present evidence of the distortion of the gas disc by ram pressure. Finally, Section 6 gives a summary of our results and conclusions.

2 OBSERVATIONS AND DATA REDUCTION

The observations of NGC 300 were carried out in late 2007 and 2008 with the six 22-m antennas of the ATCA. Five of the antennas are moveable along an east–west track with a total length of 3 km, whereas the sixth antenna is fixed and separated by another 3 km from the western end of the track.

The total observing time of 96 h was equally divided among the EW352 and EW367 array configurations to improve baseline coverage. Because of the large spatial separation between antenna 6 and all other antennas in these configurations we only used data from antennas 1 to 5 in our analysis. The resulting minimum and maximum baselines were 31 and 367 m, respectively.

NGC 300 was simultaneously observed in the 21-cm line emission of neutral hydrogen (Wild 1952) and in 21-cm radio continuum emission, using the two independent frequency chains of the ATCA. For the H\textsc{i} observations we used a bandwidth of 8 MHz centred at a frequency of 1420 MHz. The resulting velocity coverage is about 1600 km s\textsuperscript{-1} with a channel separation of 3.3 km s\textsuperscript{-1} and an effective velocity resolution of about 4 km s\textsuperscript{-1}. The radio continuum data were obtained over a bandwidth of 128 MHz centred at 1384 MHz. Only the H\textsc{i} data will be discussed in this paper.

In order to map a large field of about 2\textdegree \times 2\textdegree (corresponding to a projected size of about 65 \times 65 kpc\textsuperscript{2}) we covered NGC 300 with a large mosaic of 32 separate pointings. Adjacent pointings were separated by 16.5 arcmin which corresponds to approximately half the half-power beamwidth of the ATCA antennas at a wavelength of \(\lambda = 21\) cm. The geometry of the entire mosaic is outlined in Fig. 1. The integration time per pointing in each array

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configuration was 1.5 h. The resulting spectral rms noise level at 3.3 km s\(^{-1}\) channel separation is about 5.5 mJy per beam which is equal to the theoretical noise level.

At the beginning of each observing run we spent about 15 to 20 min on the ATCA’s standard flux calibration source, PKS 1934–638, which was used for bandpass and flux calibration of the data. Every 45 min during our observing runs we integrated for 5 min on our gain amplitude and phase calibrator, PKS 0008–421, which has a 20 cm flux of about 4.5 Jy and a separation from NGC 300 of about 9.5. PKS 0008–421 was used to calibrate gain amplitudes and phases as a function of time.

The data were reduced and analysed with the Astronomical Image Processing System (AIPS; Greisen 1990), the Multichannel Image Reconstruction, Image Analysis and Display (MIRIAD) software package (Sault, Teuben & Wright 1995) and the Groningen Image Processing System (GIPSY; Allen, Ekers & Terlouw 1985; van der Hulst et al. 1992) in a combined approach. We first used the task ATLOD to read the raw data into AIPS for the purpose of flagging bad pixels in the time-baseline domain using the interactive task SFLAG. Next, we imported the flagged data into MIRIAD. The flagging table produced by AIPS was then applied via the MIRIAD task FGFLAG before proceeding with some additional flagging of shadowed antennas, \textsc{H}\textsc{i} absorption in the primary calibrator, PKS 1934–638, and otherwise corrupted visibilities. We then carried out the standard data reduction procedure, making use of MIRIAD’s dedicated mosaicking capabilities which include automatic corrections for primary beam attenuation.

For the image cube and beam, we applied a robust weighting of visibilities with a robustness parameter of zero. The resulting synthesised beam is elliptical with a full width at half-maximum (FWHM) of 180 × 88 arcsec\(^2\) and a position angle of \(-6^\circ\) with respect to north. Furthermore, we employed a pixel size of 30 arcsec in the image domain and a resolution and channel separation of 8 km s\(^{-1}\) through Hanning smoothing in the spectral domain. The resulting spectral rms noise level is 3.5 mJy per beam, corresponding to a 5\(\sigma\) \textsc{H}\textsc{i} column density sensitivity of \(1.0 \times 10^{19}\) cm\(^{-2}\) per spectral channel. This translates into a 5\(\sigma\) \textsc{H}\textsc{i} mass sensitivity of \(1.2 \times 10^3\) \(M_\odot\) at a distance of 1.9 Mpc.

To reduce the impact of beam sidelobes caused by our incomplete aperture synthesis we subsequently deconvolved the image data cube using the \textsc{clean} algorithm originally developed by Högbom (1974). We actually applied the \textsc{steer clean} algorithm (Steer, Dewdney & Ito 1984) implemented in the \textsc{miriad} task \textsc{mosodi} with a flux density cut-off of 10 mJy per beam equivalent to about three times the rms noise level at 8 km s\(^{-1}\) channel width. Individual channel maps of the final data cube are shown in Fig. 2.

The zeroth, first and second moment maps of NGC 300 were calculated using the AIPS task \textsc{moment}. For this purpose, we first multiplied the data cube with the theoretical gain across the mosaic to obtain a data cube with a constant noise level at all positions and frequencies. Next, we created a mask from the data cube by Hanning smoothing the frequency axis over three channels, convolving the spatial dimension with a Gaussian of 5 pixels FWHM, and then masking all pixels in the smoothed cube that had a flux density value of less than 4.5 mJy per beam. In \textsc{moment}, only those pixels of the original data cube that had not been masked in the smoothed cube were used in calculating the moment maps. Finally, the moment maps were divided again by the gain model to recover the original gain levels across the mosaic.

There are several ways of determining the mean radial velocity of an \textsc{H}\textsc{i} line, including the calculation of the first moment of the spectrum, the fitting of one or more Gaussian functions to the spectral line or simply by using the velocity of the peak of the \textsc{H}\textsc{i} line. The impact of these and other methods on the outcome of rotation curve fits was studied in detail by de Blok et al. (2008) based on a sample of galaxies observed as part of The \textsc{H}\textsc{i} Nearby Galaxy Survey (THINGS; Walter et al. 2008). They found the most suitable method to be the fitting of Gauss–Hermite polynomials (van der Marel & Franx 1993) with an additional skewness parameter, \(h_3\), to the spectral lines. The fitting function used by de Blok et al. (2008) and implemented in the \textsc{gipsy} task \textsc{xgaufit} is a modified Gauss–Hermite polynomial including only the zeroth- and third-order terms, namely

\[
A(y) = a \exp\left(-\frac{y^2}{2}\right) \left(1 + h_3 \frac{2y^3 - 3y}{\sqrt{3}}\right)
\]  

with the substitution \(y = (x - b)/c\). The free parameters of the fit are \(a, b, c,\) and the aforementioned skewness parameter, \(h_3\). The advantage of using Gauss–Hermite polynomials instead of pure Gaussian functions is that the former will account for asymmetries in the line profile that can be characterized by \(h_3\). In our analysis we used the position of the maximum of \(A(y)\) to derive the radial velocity field.

3 RESULTS

3.1 General parameters

The total \textsc{H}\textsc{i} column density map of NGC 300, derived from the zeroth moment of the data cube, is shown in Fig. 3.\(^1\) The \textsc{H}\textsc{i} disc appears to be significantly more extended than the optical disc and shows a clear separation into an inner and outer disc. The inner disc

\(^1\) Note that the assumption was made that the \textsc{H}\textsc{i} gas is optically thin. In the innermost regions of NGC 300 this assumption may not be valid, and the true column densities may be higher.
Figure 2. Channel maps of the ATCA H\textsc{i} data cube of NGC 300 in the range of $v_{\text{LSR}} = 16$ to $248$ km s$^{-1}$ (corresponding to barycentric velocities of 24 to 256 km s$^{-1}$). The grey-scale images range from $-20$ to $+100$ mJy per beam. The contour levels are $-15$ (dashed), 15, 50, 150 and 500 mJy per beam. The increased noise along the edges of the maps is the result of primary beam attenuation. Channels containing Galactic H\textsc{i} emission were not deconvolved.

is characterized by high column densities of $N_{\text{H}} \gtrsim 5 \times 10^{20}$ cm$^{-2}$ and appears to be aligned with the stellar disc. In contrast, the outer disc has lower column densities of typically $N_{\text{H}} \lesssim 2 \times 10^{20}$ cm$^{-2}$ and is spatially much more extended. Furthermore, the transition between the inner and outer disc seems to go along with a systematic twist resulting in very different orientation angles of the two discs. This twist is also evident in the radial velocity map in Fig. 3 and the position-velocity diagrams in Fig. 4.

Owing to our large mapping area and sufficiently high sensitivity, this is the first time that the entire extent (down to a column density...
level of about \(10^{19}\, \text{cm}^{-2}\) of the H\(_i\) disc of NGC 300 has been revealed in such detail. Within the \(10^{19}\, \text{cm}^{-2}\) column density level, the major axis of the H\(_i\) disc of NGC 300 spans slightly more than 1° on the sky which is equivalent to a linear diameter of about 35 kpc. Earlier H\(_i\) observations of NGC 300 with the VLA by Puche et al. (1990) revealed only a small part of the outer disc, mainly due to the insufficient size of their mosaic of only five pointings.

The integrated H\(_i\) spectrum of NGC 300 is shown in Fig. 5. The total flux derived from our ATCA data is 1720 Jy km s\(^{-1}\). The corresponding total H\(_i\) mass of NGC 300 amounts to \(M_{\text{H}_i} = 1.5 \times 10^9\, \text{M}_\odot\) under the assumption that the gas is optically thin. Since this will not be the case in the dense inner regions of the disc, the derived mass must be considered a lower limit. The effect of missing short spacings and the inability of CLEAN to recover all the flux is visible in the channel maps of Fig. 2, with the H\(_i\) emission sitting in a slightly negative bowl.

The H\(_i\) mass determined from the H\(_i\) Parkes All-Sky Survey (HIPASS; Barnes et al. 2001) is slightly larger with \(M_{\text{H}_i} = (1.69 \pm 0.13) \times 10^9\, \text{M}_\odot\) (scaled to a distance of 1.9 Mpc; Koribalski et al. 2004). This indicates that some flux is missing in our ATCA observations, although not much. On the other hand, HIPASS suffers from inaccurate bandpass calibration resulting in serious artefacts near bright and extended sources, and the true H\(_i\) mass of NGC 300 could even be somewhat higher than the one determined by Koribalski et al. (2004). The total H\(_i\) mass of \(8 \times 10^8\, \text{M}_\odot\) determined by Puche et al. (1990) from their VLA observations (again scaled to a distance of 1.9 Mpc) is significantly smaller, mainly reflecting the limited size of their mosaic on the sky and possibly the lack of short telescope baselines.

We can also try to assess how the mass is distributed between the inner and outer disc of NGC 300. By simply defining a column density boundary of \(N_{\text{H}_i} = 5 \times 10^{20}\, \text{cm}^{-2}\) between the two disc components we obtain H\(_i\) masses of \(8.5 \times 10^8\) and \(6.5 \times 10^8\, \text{M}_\odot\) for the inner and outer disc, respectively. Hence, a significant fraction of the H\(_i\) mass is within the extended outer disc.
A closer inspection of the column density distribution reveals a certain degree of asymmetry in the disc. The south-eastern edge of the disc is rather clean and sharp, whereas the north-western edge looks more frayed and less well defined. This is illustrated in Fig. 6 showing the H\textsc{i} column density profile across NGC 300 as a function of declination offset (i.e., along a line of constant right ascension passing through the centre of the galaxy). There is a distinctive plateau in the southern part of NGC 300 followed by a sudden and steep drop in column density towards the southern edge of the disc. In the northern part, in contrast, we observe a steady exponential decline without any obvious plateau or drop.

The velocity dispersion map of NGC 300, derived from the fitting of Gauss–Hermite polynomials to the H\textsc{i} spectra, is shown in the lower-right panel of Fig. 3. Velocity dispersions across the inner disc are variable and somewhat higher than in the outer disc with typical values in the range of about 10 to 15 km s$^{-1}$. In contrast, the outer disc appears homogeneous with dispersions of just under 10 km s$^{-1}$ in most areas (equivalent to just over 20 km s$^{-1}$ FWHM for Gaussian line profiles). These values are not atypical for the warm neutral medium of the Milky Way (Kalberla & Kerp 2009) and indicate an upper limit of the order of $10^4$ K for the gas temperature. The true gas temperature may be well below this upper limit, as effects such as turbulent motion and beam smearing will contribute to the observed linewidth.

Fig. 7 reveals regions of increased velocity dispersion near the boundary between the inner and outer H\textsc{i} disc, in particular on the north-eastern side of the galaxy. The highest dispersions of about...
20 km s$^{-1}$ are found along a filament in the eastern part of NGC 300. Such high values can no longer be explained by thermal line broadening alone, as in that case gas temperatures of about $5 \times 10^4$ K would be required. Instead, the high-velocity dispersion suggests the presence of different gas components along the line of sight as supported by the spectra shown on the right-hand side of Fig. 7. The spectra were extracted from the locations of highest dispersion marked with A and B in the map and reveal a clear double line profile at the boundary between the inner and outer H$\alpha$ disc. Obviously, each disc component produces a separate line component in the spectrum, and the transition between the inner and outer disc is not gradual but abrupt within the size of our synthesized beam. This is also suggested by the radial velocity field as indicated by the white contours in Fig. 7. In the transition region between the inner and outer disc we observe a strong discontinuity in the velocity field. The resulting kinks in the velocity contours coincide precisely with the regions of increased velocity dispersion in the map, thus confirming our impression of an abrupt transition between the inner and outer disc of NGC 300.

Interestingly, the transition from the inner disc to the outer disc is less sharp on the south-western side of NGC 300 where the velocity contour lines are much smoother, and – despite a slightly increased velocity dispersion – the spectra do not exhibit a double-peak profile. Instead, there is a gradual transition from the inner to the outer disc component in the spectrum across several beam widths.

### 3.2 Rotation curve

In order to determine the rotation curve, $v_{\text{rot}}(r)$, of NGC 300 we must assume a model for the three-dimensional kinematics of the galaxy. One of the simplest and most commonly applied models is to assume that the gas particles move in circular orbits along tilted rings with varying position angle, $\phi$, and inclination, $i$ (e.g., Rogstad, Lockhart & Wright 1974). In addition, each ring is assigned a position, $(x_0, y_0)$, and systemic velocity, $v_{\text{sys}}$, both of which can also be allowed to vary.

We used the GIPSY task ROTCUR to fit a tilted ring model to the radial velocity field of NGC 300 as derived from the fitting of Gauss–Hermite polynomials to the spectral lines. We fitted 20 rings with radii ranging from $r = 100$ to 2000 arcsec (0.9 to 18.4 kpc) in steps of 100 arcsec. Each ring was chosen to be 100 arcsec wide to match the angular resolution of our data. Data within an angle of $\pm 20^\circ$ around the minor axis of NGC 300 were excluded from the fit, and all data were weighted with the cosine of the position angle, $|\cos(\phi)|$.

We first derived the position of the centre of NGC 300 from an optical V-band image taken with the MPG/ESO 2.2-m telescope at La Silla (Pietrzyński et al. 2002). NGC 300 has a very distinct, point-like core that is thought to be associated with either a nuclear stellar cluster or even a central black hole (Soffner et al. 1996; Kim et al. 2004) and should therefore provide us with an accurate position of the dynamical centre. A Gaussian fit to the optical core revealed a central position of $\alpha = 00^h54^m53.4^s$ and $\delta = -37^\circ41'02.6''$ in the J2000.0 coordinate system.2 Next, we ran ROTCUR with the optically derived central position fixed and the gas expansion velocity also fixed to a value of $v_{\text{exp}} = 0$ km s$^{-1}$. All other parameters (systemic velocity, rotation velocity, position angle and inclination angle) were still left as free parameters. After the first run of ROTCUR we determined the systemic velocity by averaging over the fitted systemic velocities of all rings. The resulting value of $v_{\text{sys}} = 136 \pm 2$ km s$^{-1}$ in the LSR frame, corresponding to $144 \pm 2$ km s$^{-1}$ in the barycentric reference frame, was then used and kept fixed in all subsequent runs. This result is consistent with the barycentric velocity of $v_{\text{sys}} = 146 \pm 2$ km s$^{-1}$ found by Koribalski et al. (2004) based on HIPASS.

Next, we ran ROTCUR again with only the rotation velocity, position angle and inclination angle left as free parameters. We followed the approach described by de Blok et al. (2008) and first fixed the radial position angle profile. To reduce the initial bumpiness of the position angle profile we smoothed it by applying a boxcar filter

2This position is consistent with the dynamical centre of the innermost tilted rings as derived by ROTCUR.
with a width of 300 arcsec (equal to three radial bins) to the position angle solution. After the next run of \textsc{rotcur} we also smoothed and fixed the inclination angle profile using the same boxcar filter as for the position angle. With all other parameters fixed, we then ran \textsc{rotcur} for the last time to obtain the final solution for the rotation curve.

Our final H$_{\text{i}}$ rotation curve of NGC 300 is shown in Fig. 8(a) and Table 2. A comparison between the observed and modelled velocity fields is presented in Fig. 9. Due to the combination of a large field of view with a fairly compact array configuration we are able to determine the rotation curve out to an angular radius of 2000 arcsec equivalent to a physical radius of 18.4 kpc. This is a significant improvement compared to the previous measurement with the VLA by Puche et al. (1990) which covered a radius of only 11 kpc. The rotation curve derived by Puche et al. (1990) is also plotted in Fig. 8(a) for comparison. Within their uncertainties both rotation curves agree quite well, although a direct comparison is difficult due to the different resolutions of the VLA observations and the ATCA observations presented here. At a higher resolution of 50 arcsec FWHM, the rotation curve of Puche et al. (1990) shows small-scale variations not present in our ATCA rotation curve. In addition, there is some discrepancy in the very inner region of $r < 5$ arcmin which is most likely caused by different degrees of beam smearing in combination with a rapid change in rotation velocity in the inner part of the galaxy. Hence, our ATCA observations in particular are not capable of reliably defining the rotation curve of NGC 300 across the inner 3 kpc.

The derived rotation curve of NGC 300 rises out to a radius of about 15 to 20 arcmin (equivalent to 8 to 11 kpc) where we observe a maximum rotation velocity of $v_{\text{rot}} = 98.8 \pm 3.3$ km s$^{-1}$ at $r = 16.7$ arcmin (9.2 kpc). This value is consistent with the results of Puche et al. (1990) who found a maximum velocity of $v_{\text{rot}} = 97.0 \pm 5.7$ km s$^{-1}$ at a radius of 15.8 arcmin (8.7 kpc). Rogstad et al. (1979) derived similar values in the range of $v_{\text{rot}} = 94$ to 102 km s$^{-1}$ at a radius of 16 arcmin (8.8 kpc). Beyond about 10 kpc the rotation velocity gradually decreases to below 85 km s$^{-1}$. This decrease was not seen in the previous VLA data of Puche et al. (1990) due to insufficient radial extent of their map.

A particular problem of rotation curve fits in general is the determination of uncertainties. The statistical errors of the fit, as provided by \textsc{rotcur}, are usually much smaller than the actual uncertainties of the solution which are dominated by systematic errors such as non-circular motion of the observed gas, insufficient spatial resolution of the observations, effects of varying optical depth, etc. There are two possible ways to obtain more reliable estimates of the uncertainties. One possibility is to determine the standard deviation of velocities along each tilted ring from the mean value of the rotation velocity for that ring. This provides us with a more realistic assessment of the true deviations of the observed velocities from the model. The error bars of our final rotation curve presented in Fig. 8(a) have been determined by this method.

Another possibility is to derive the rotation curve for the approaching and receding side of the galaxy separately and assess the differences between the two curves. This is shown in Fig. 8(b) where
Table 2. Modelling parameters of NGC 300. The columns denote: galactocentric radius, \( r \), in arcsec and kpc; derived rotation velocity, \( v_{\text{rot}} \); tilted ring position angle, \( \psi \), and inclination, \( i \); stellar mass surface density, \( \Sigma_* \), as derived from the \textit{Spitzer} IRAC 3.6 \( \mu \)m, 4.5 \( \mu \)m and combined data; gas mass surface density, \( \Sigma_{\text{gas}} \).

| \( r \) (arcsec) | \( r \) (kpc) | \( v_{\text{rot}} \) (km s\(^{-1}\)) | \( \psi \) (°) | \( i \) (°) | \( \Sigma_{*} \) (M\(_{\odot}\) pc\(^{-2}\)) | \( \Sigma_{*} \) (M\(_{\odot}\) pc\(^{-2}\)) | \( \Sigma_{\text{gas}} \) (M\(_{\odot}\) pc\(^{-2}\)) |
|----------------|-------------|-----------------|--------|--------|----------------|----------------|----------------|
| 100            | 0.92        | 43.3 ± 4.7      | 290.6  | 39.9   | 45.4 ± 5.9    | 41.8 ± 6.1    | 43.6 ± 4.3    |
| 200            | 1.84        | 66.5 ± 3.1      | 289.3  | 40.5   | 24.3 ± 3.3    | 22.8 ± 3.5    | 23.5 ± 2.4    |
| 300            | 2.76        | 75.4 ± 2.7      | 289.5  | 42.6   | 10.8 ± 1.6    | 10.1 ± 1.7    | 10.4 ± 1.2    |
| 400            | 3.68        | 80.3 ± 2.1      | 290.2  | 44.6   | 6.3 ± 1.1     | 6.2 ± 1.2     | 6.3 ± 0.8     |
| 500            | 4.61        | 83.5 ± 2.2      | 289.9  | 45.8   | 3.7 ± 1.0     | 3.7 ± 0.9     | 3.7 ± 0.7     |
| 600            | 5.53        | 88.4 ± 2.9      | 290.5  | 46.5   | 1.5 ± 0.7     | 1.7 ± 0.6     | 1.6 ± 0.4     |
| 700            | 6.45        | 92.2 ± 3.3      | 293.2  | 49.0   | 0.5 ± 0.4     | 0.5 ± 0.5     | 0.5 ± 0.3     |
| 800            | 7.37        | 95.7 ± 3.3      | 297.8  | 51.0   | 0.2 ± 0.4     | 0.1 ± 0.6     | 0.1 ± 0.3     |
| 900            | 8.29        | 96.8 ± 3.1      | 304.4  | 51.3   | 0.1 ± 0.4     | −0.1 ± 0.4    | 0.0 ± 0.3     |
| 1000           | 9.21        | 98.8 ± 3.1      | 311.1  | 49.9   | 0.1 ± 0.4     | −0.1 ± 0.5    | 0.0 ± 0.3     |
| 1100           | 10.13       | 98.3 ± 3.8      | 316.4  | 49.3   | 0.0 ± 0.5     | −0.1 ± 0.5    | 0.0 ± 0.3     |
| 1200           | 11.05       | 95.4 ± 3.5      | 319.4  | 49.7   | 0.0 ± 0.6     | 0.1 ± 0.5     | 0.0 ± 0.4     |
| 1300           | 11.98       | 92.8 ± 3.0      | 321.6  | 49.9   | −0.1 ± 0.5    | 0.0 ± 0.4     | 0.0 ± 0.3     |
| 1400           | 12.90       | 90.7 ± 3.3      | 324.2  | 48.9   | 0.0 ± 0.5     | 0.1 ± 0.5     | 0.0 ± 0.4     |
| 1500           | 13.82       | 89.1 ± 3.3      | 327.1  | 47.0   | –             | –             | 0.8 ± 0.3     |
| 1600           | 14.74       | 87.8 ± 2.9      | 329.6  | 46.6   | –             | –             | 0.6 ± 0.3     |
| 1700           | 15.66       | 88.4 ± 3.4      | 331.4  | 45.3   | –             | –             | 0.4 ± 0.2     |
| 1800           | 16.58       | 89.1 ± 3.8      | 331.9  | 44.3   | –             | –             | 0.3 ± 0.1     |
| 1900           | 17.50       | 87.3 ± 3.1      | 332.0  | 42.7   | –             | –             | 0.2 ± 0.1     |
| 2000           | 18.42       | 82.7 ± 2.7      | 331.7  | 43.3   | –             | –             | 0.1 ± 0.1     |

Figure 9. Panel (a) shows the observed radial velocity field of NGC 300 based on the position of the intensity maximum of Gauss–Hermite polynomials fitted to the spectral line profiles. Panel (b) shows the modelled radial velocity field derived from the overall rotation curve as shown in Fig. 8. In both panels, the contour lines are drawn in intervals of 15 km s\(^{-1}\) centred about the systemic velocity of \( v_{\text{LSR}} = 136 \text{ km s}^{-1} \) (bold contour line; equivalent to 144 km s\(^{-1}\) in the barycentric reference frame). All velocities in the two maps are given in the LSR frame. Panel (c) shows the difference between the observed and modelled velocity fields. The contour lines are drawn at levels of ±4, ±8, ±12 and ±16 km s\(^{-1}\). The black, dotted ellipse in all three maps marks the outer edge of the model and illustrates the significant lopsidedness of the gas disc of NGC 300.

The approaching and receding curves are compared to the overall rotation curve. The fits for the approaching and receding sides are independent of the overall rotation curve fit, as we derived separate solutions for the position angle and inclination. The two rotation curves both show a clear maximum and then decrease again at larger radii. The position of the maximum and the overall shape of the rotation curve, however, differ significantly between the approaching and receding side. These discrepancies indicate systematic uncertainties of up to ±10 km s\(^{-1}\) for the overall rotation curve of NGC 300. The rotation curve of the receding side continues to decrease after reaching a maximum at \( r \approx 10 \text{ kpc} \), whereas the curve derived from the approaching side also decreases but then flattens out at larger radii. In addition, the approaching side has its rotation curve maximum significantly further inwards at \( r \approx 6.5 \text{ kpc} \). These differences indicate a high degree of asymmetry in the kinematics of the gas disc of NGC 300, some of which is immediately evident from the velocity map in the left-hand panel of Fig. 9. The results indicate that the finding of a decreasing rotation curve in the outer disc should be approached with caution because non-circular motions and asymmetries in the disc could have contributed significantly to the observed velocity field of NGC 300.

Figs (c) and (d) show the position angle, \( \psi(r) \), and inclination, \( i(r) \), used in the final rotation curve fit with \textsc{rotcur}. For comparison we also show the originally fitted values before applying the boxcar filter for smoothing and the separate solutions for the approaching and receding side of the galaxy. The position angle is constant over the entire inner disc of NGC 300 with \( \psi(r) = 290^\circ \) for \( r \lesssim 10 \text{ arcmin} \). Beyond the edge of the inner disc the position angle of the gas disc gradually changes by about 40° only to become constant again in the very outer disc with \( \psi(r) = 332^\circ \) for \( r \gtrsim 30 \text{ arcmin} \).
This behaviour of \( \varphi(r) \) reflects the visual impression of a twist in the \( \text{H} \text{I} \) disc of NGC 300 and suggests the presence of two distinct gas discs, each with its own spatial orientation. The variation in inclination, \( i(r) \), with radius appears less regular. The inclination of the gas disc increases from about 40° to just over 50° within the inner 15 arcmin (8 kpc) and then gently decreases again to \( i(r) \lesssim 45° \) in the outermost regions of the disc.

The observed decrease in rotation velocity is strongly coupled with the characteristics of the inclination angle in the outer parts of the disc. A smaller inclination angle would result in a higher rotation velocity. In order to obtain a flat rotation curve, the inclination angle of the outermost tilted ring would need to be about 35°. This is significantly smaller than the inclination angle of about 43° resulting from the tilted ring model. At the same time, we estimate a geometric inclination angle of about 44° by comparing the major and minor axis of the 2 \( \times \) 10\(^{19} \) cm\(^{-2} \) \( \text{H} \text{I} \) column density contour level under the assumption of perfect circular symmetry of the disc. This is consistent with the kinematic inclination from the tilted ring model.

It is interesting to note in this context that the maximum rotation velocity occurs near the transition radius between the inner and outer \( \text{H} \text{I} \) disc. A closer inspection of the rotation curves derived for the approaching and receding sides of NGC 300 (Fig. 8) reveals that the position of maximum rotation velocity is closely linked to strong variations in inclination angle at that particular radius. It is possible that part of this variation in inclination is an artefact caused by the failure of the tilted ring model to cope with the sudden transition between the inner and outer disc. Consequently, the decrease in rotation velocity across the outer disc of NGC 300 could be less pronounced than indicated by the tilted ring model.

### 4 MASS MODELS

After having determined the overall rotation curve, we can now try to derive mass models of NGC 300 using the GIPSY task \textsc{rotmas}. This will allow us to study the radial distribution of the different visible and dark matter components in NGC 300 and assess how much dark matter is required to explain the rotation curve. For this purpose, we assume the presence of three mass components, namely a gaseous disc, a stellar disc and a dark matter halo. \textsc{rotmas} will attempt to fit the velocity curves of these three components to the total rotation curve:

\[
v_{\text{rot}}^2(r) = f_{\text{gas}}v_{\text{gas}}^2(r) + f_{\text{stellar}}v_{\text{stellar}}^2(r) + v_{\text{DM}}^2(r).
\]

The factors \( f_{\text{gas}} \) and \( f_{\text{stellar}} \) are mass scaling factors for the stellar and gaseous disc, respectively. \textsc{rotmas} determines the velocity curve, \( v(r) \), of a mass component from its mass surface density, \( \Sigma(r) \). In the following Sections 4.1 and 4.2, we will derive the required mass surface densities of the gaseous and stellar disc. In Section 4.3, we will introduce the different dark matter models used in the mass modelling of NGC 300. Finally, Section 4.4 will discuss the outcome of the mass modelling.

#### 4.1 Gaseous component

Deriving the radial mass distribution of the gaseous disc in NGC 300 is relatively straightforward. We first used the GIPSY task \textsc{ellint} to derive the radial \( \text{H} \text{I} \) column density profile from the column density map, using the tilted ring parameters obtained from the rotation curve fit with \textsc{rotcur}. The column density profile, \( N_{\text{HI}}(r) \), can then be converted into gas mass surface density via

\[
\Sigma_{\text{gas}}(r) = f_{\text{HI}}N_{\text{HI}}(r)\cos(i),
\]

where \( m_{\text{H}} = 1.674 \times 10^{-27} \) kg is the mass of a hydrogen atom, and \( f \) is a mass correction factor. For our analysis, we assume a value of \( f = 1.4 \) to account for primordial helium expected to be associated with the neutral hydrogen gas in the disc of NGC 300.

The factor \( \cos(i) \) is required to de-project all column densities to face-on values. The resulting mass surface density profile of the gas disc is shown in Fig. 10 and Table 2.

Throughout the inner part of the gas disc, the surface density is basically constant with \( \Sigma_{\text{gas}} \approx 7\ M_{\odot} \text{pc}^{-2} \) (including the correction for helium). Beyond a radius of about 6 kpc, the gas mass surface density begins to decline. The outer profile can be reasonably well described by an exponential decline, \( \Sigma_{\text{gas}} \propto \exp(-r/h) \), with a radial scalelength of \( h = 3.44 \pm 0.15 \) kpc or a power law, \( \Sigma_{\text{gas}} \propto r^{1}, \) with a slope of \( a = -2.38 \pm 0.07 \).

This method, of course, assumes that the \( \text{H} \text{I} \) gas is optically thin which might not be the case for the densest regions along the spiral arms of NGC 300. As a consequence, column densities, and hence gas mass surface densities, in these regions would be underestimated. In addition, we have made the assumption that the gas disc is infinitely thin, and any significant thickness of the disc would result in errors in the determination of \( \text{H} \text{I} \) column densities, depending also on the inclination angle of the disc.

#### 4.2 Stellar component

Deriving the stellar mass distribution in NGC 300 is significantly more complicated. In order to determine the radial mass profile of the stellar component of NGC 300 and its contribution to the derived rotation curve, we need to find a way to convert the optical or near-infrared flux density profile, \( S_{\lambda}(r) \), into stellar mass surface density, \( \Sigma_{\star}(r) \), via the stellar mass-to-light ratio, \( \Upsilon_{\star} \), such that

\[
\Sigma_{\star}(r) \sim \Upsilon_{\star} S_{\lambda}(r).
\]

The index \( \lambda \) indicates that both the mass-to-light ratio and the flux density are wavelength-dependent and are usually determined within a specific photometric band of wavelength \( \lambda \).

By using near-infrared instead of optical data one can largely overcome the problem of absorption by dust in the measurement of the radial flux density profile of the stellar component. NGC 300 has been observed with the Infrared Array Camera (IRAC) on board the Spitzer Space Telescope (Helou et al. 2004), and for this work we have used IRAC data in the 3.6 and 4.5 \( \mu \)m bands to determine the stellar surface brightness profile. The nominal wavelengths of these two bands are 3.550 and 4.493 \( \mu \)m, respectively (Fazio et al. 2010).
The density profile, $\Sigma_\star(r)$, in the 3.6 and 4.5 $\mu$m wavebands must then be converted to stellar mass density, $\Sigma_\star(r)$, using the stellar mass-to-light ratio in units of the solar value, $\Sigma_\star = \Sigma_\star / \Sigma_\odot$. The corresponding conversion formula in equation (4) can be rewritten in the form

$$\Sigma_\star(r) = C_\lambda \gamma r_a f_a S_\lambda(r) / S_0$$

where $C_\lambda$ is a wavelength-dependent conversion factor, $f_a$ is the wavelength-dependent aperture correction factor for extended sources in IRAC images and $S_0$ denotes the wavelength-dependent zero-magnitude flux. Based on the calculations of Oh et al. (2008) we derive conversion factors in the 3.6 and 4.5 $\mu$m wavebands of

$$C_{3.6} = 0.196 M_\odot pc^{-2},$$

$$C_{4.5} = 0.201 M_\odot pc^{-2}.$$

(5)

According to Reach et al. (2005), the aperture correction factors for the 3.6 and 4.5 $\mu$m bands are $f_a = 0.944$ and 0.937, respectively, and the corresponding zero-magnitude fluxes are $S_0 = 280.9 \pm 4.1$ and 179.7 $\pm 2.6$ Jy.

Before we can use equation (5) to convert radial flux density profiles into stellar mass density profiles we first need to determine the stellar mass-to-light ratio in NGC 300. Determination of the stellar mass-to-light ratio is very difficult because it depends on several uncertain parameters such as the initial mass function (IMF) of NGC 300, its star formation history, metallicity, etc. To make matters worse, most of these parameters will change with growing distance from the centre of a galaxy, resulting in a radial variation, $\gamma_\star(r)$, of the stellar mass-to-light ratio.

Colour indices provide a convenient way to determine the mass-to-light ratio through basic photometric measurements. Bell & de Jong (2001) used galaxy evolution models to explore the relation between stellar mass-to-light ratio and optical/near-infrared colours of galaxies. They found a strong and robust correlation between the stellar mass-to-light ratio and the integrated colour of the stellar population in their model galaxies. They also concluded that a modified Salpeter (1955) IMF with a smaller fraction of low-mass stars is consistent with the observed stellar mass-to-light ratios of a sample of spiral galaxies used for comparison with the models. From the relations between mass-to-light ratio and colour found by Bell & de Jong (2001) we derive the following relation between the $K$-band stellar mass-to-light ratio, $\gamma_k$, and the $J - K$ colour index:

$$\log_{10}(\gamma_k) = 1.434 (J - K) - 1.380.$$ 

(8)

The relation was derived using the mass-dependent formation epoch model with bursts and the modified Salpeter IMF adopted by Bell & de Jong (2001). Since our surface brightness measurements are based on Spitzer data, we have to convert $\gamma_k$ into the stellar mass-to-light ratios derived for the Spitzer IRAC bands of 3.6 and 4.5 $\mu$m. Using stellar population synthesis models, Oh et al. (2008) found the following well-defined correlations:

$$\gamma'_{3.6} = 0.92 \gamma_k - 0.50,$$

$$\gamma'_{4.5} = 0.91 \gamma_k - 0.08.$$ 

(9)

(10)

With the set of equations derived above we now have all tools at hand to determine the stellar surface density of NGC 300.

From the Two Micron All Sky Survey (2MASS) Large Galaxy Atlas (Jarrett et al. 2003) we derive a global colour index of $J - K = 0.646 \pm 0.033$ mag for NGC 300. Inserting this value into equation (8) yields a stellar mass-to-light ratio for NGC 300 in the $K$ band of

$$\log_{10}(\gamma_k) = -0.454 \pm 0.047.$$ 

(11)

Using equations (9) and (10), we derive stellar mass-to-light ratios in the IRAC 3.6 and 4.5 $\mu$m bands of

$$\log_{10}(\gamma'_{3.6}) = -0.564 \pm 0.055,$$

$$\log_{10}(\gamma'_{4.5}) = -0.620 \pm 0.054.$$ 

(12)

(13)

We can now use equation (5) to derive the stellar mass surface density of NGC 300. Again, we used the GIPSY task ELLINT with the tilted ring fitting parameters derived earlier to determine the surface brightness profiles of NGC 300 from the Spitzer 3.6 and 4.5 $\mu$m images. Both profiles were then corrected for inclination and combined into a single stellar mass surface density profile which is shown in Fig. 10 and Table 2. The resulting total stellar mass is $(1.0 \pm 0.1) \times 10^9 M_\odot$.

The derived profile can be described by an exponential decline, $\Sigma_\star(r) \propto \exp(-r/r_c)$, with a radial scalelength of $r_c = 1.39 \pm 0.04$ kpc. This value is in good agreement with the scalelength of 1.38 kpc measured in the $I$ band by Kim et al. (2004). Comparison with the values of 2.06 kpc in the $B_1$ band (Carignan 1985) and 1.94 kpc in the $B$ band (Kim et al. 2004) suggests that the outer stellar disc of NGC 300 is bluer than the inner disc.

As mentioned earlier, we cannot expect the stellar mass-to-light ratio to be constant across the entire galaxy, but there will likely be a radial variation in $\gamma_k$ reflecting different star formation histories and stellar populations at different distances from the centre of NGC 300. A way to account for this radial variability of $\gamma_k$ would be to determine the radial profile of the $J - K$ colour index of NGC 300 based on infrared imaging data. Unfortunately, the signal-to-noise ratio in the 2MASS images is very low, and determination of $\gamma_k$ as a function of galactocentric distance is therefore not feasible due to large uncertainties.

4.3 Dark matter component

4.3.1 Pseudo-isothermal halo

The spherical pseudo-isothermal halo is one of the simplest models for the density profile of dark matter haloes. Its density profile resembles that of an isothermal sphere and reads

$$\rho(r) = \frac{\rho_0}{1 + (r/r_c)^2}.$$ 

(14)

(e.g. Begeman, Broeils & Sanders 1991) where $\rho_0$ is the central density of the halo and $r_c$ the so-called core radius. The corresponding velocity profile is

$$v^2(r) = 4\pi G \rho_0 r_c^3 \left(1 - \frac{r_c}{r} \arctan \left(\frac{r}{r_c}\right)\right).$$ 

(15)

(Kent 1986).

4.3.2 Burkert halo

For his study of dwarf galaxy rotation curves Burkert (1995) introduced the following empirical halo density profile:

$$\rho(r) = \frac{\rho_0 r_c^3}{(r + r_c)(r^2 + r_c^2)}.$$ 

(16)
Again, $\rho_0$ and $r_c$ are the central density and core radius of the halo, respectively. The resulting velocity profile reads

$$v^2(r) = \frac{6.4G\rho_0 r^3}{r} \left[ \ln \left( 1 + \frac{r}{r_c} \right) + \frac{1}{2} \ln \left( 1 + \frac{r^2}{r_c^2} \right) - \arctan \left( \frac{r}{r_c} \right) \right]$$

(Salucci & Burkert 2000). The major difference between the Burkert halo and the pseudo-isothermal halo is that for large radii the Burkert halo density behaves as $\rho(r) \sim r^{-3}$, whereas for the pseudo-isothermal halo we get a different behaviour of $\rho(r) \sim r^{-2}$.

### 4.3.3 NFW halo

The NFW dark matter density profile was suggested by Navarro, Frenk & White (1995, 1996) based on numerical simulations of dark matter haloes in a hierarchically clustering universe. They found that in their models the radial density profile of dark matter haloes can be accurately described by

$$\rho(r) = \frac{\Delta \rho_{200}}{r_c} \left( 1 + \frac{r}{r_c} \right)^{-1}$$

(17)

where $\Delta \rho_{200}$ is the critical density of the Universe, $r_c$ is the so-called characteristic, dimensionless density of the halo, and $r_s$ is a scale radius. According to Navarro, Frenk & White (1997), the resulting circular velocity curve of the dark matter halo reads

$$v^2(r) = \frac{v_{200}^2}{x} \ln(1 + cx) - \frac{cx}{1 + cx}$$

(19)

with the substitution $x = r/r_{200}$ and the concentration parameter $c = r_{200}/r_s$ (not to be confused with the speed of light, c). In this form of the equation, $r_{200}$ denotes the radius within which the mean density of the halo equals 200 times the critical density of the Universe, $\Delta \rho_{200} = 3H_0^2/(8\pi G)$. This choice is somewhat arbitrary, although $r_{200}$ corresponds to approximately the virial radius of the halo. Accordingly, $v_{200}$ is the circular velocity of the halo at $r_{200}$ expressed by

$$v_{200} = \sqrt{\frac{GM_{200}}{r_{200}}} = 10H_0 r_{200}.$$  

(20)

This leaves us with only two free parameters for the rotation curve fit, namely $r_s$ and $r_{200}$. In addition, we assumed a Hubble constant of $H_0 = 70.5$ km s$^{-1}$ Mpc$^{-1}$ (Hinshaw et al. 2009) throughout this paper. Note that the NFW density profile has a singularity at the centre of the halo. Nevertheless, both the mass and circular velocity are well-defined and finite at all radii.

### 4.4 Mass modelling of NGC 300

Throughout the literature, there has been no consistent approach as to what vertical density profile, $\rho(z)$, to assume for the gaseous and stellar discs. Capozziello, Cardone & Troisi (2007), for example, assumed both discs to be infinitely thin, whereas de Blok et al. (2008) assumed an infinitely thin gas disc but a sech$^2(z/z_0)$ distribution for the stellar disc. Sanders & Noordermeer (2007), in turn, also assumed the gas disc to be extended in the vertical direction with the same thickness as that of the stellar disc. In contrast to all these approaches, Kalberla et al. (2007) demonstrated that the HI disc of the Milky Way shows strong flaring, with the scaleheight (half width at half maximum) increasing from $z_0 = 60$ pc at a radius of 4 kpc up to $z_0 \approx 2.7$ kpc at a radius of 40 kpc.

The sech$^2(z/z_0)$ distribution of the stellar disc is motivated by studies of edge-on spiral galaxies by van der Kruit & Searle (1981a,b). They found that the mass density of the stellar disc is of the form

$$\rho(r, z) = \rho(r) \text{sech}^2(z/z_0)$$

(21)

with the scaleheight, $z_0$, being largely independent of radius, $r$ [but see de Grijs & Peletier (1997) for evidence of a variation of $z_0$ with $r$]. We adopt this distribution in our model of NGC 300 and assume a ratio of $h/z_0 = 5$ in accordance with previous studies (e.g. van der Kruit & Searle 1981a). From the exponential scalelength, $h = 1.39 \pm 0.04$ kpc, of the combined 3.6 and 4.5 $\mu$m mass surface density profile we therefore derive a vertical scaleheight of $z_0 \approx 280$ pc.

As for the gaseous disc, we have considered two cases, namely an infinitely thin disc and an exponential distribution with a scaleheight equivalent to that of the stellar disc. It turns out that a thicker gas disc results in a slightly lower rotation velocity and a general smoothing of the velocity profile of the gaseous component. However, the introduction of a non-zero scaleheight for the gaseous disc does not have any significant influence on the mass modelling as long as the scaleheight is not larger than a few hundred pc. We therefore decided to make the assumption of an infinitely thin gas disc in all our models.

For all three halo models we carried out fits for fixed, partly fixed (gas only), and variable stellar and gaseous mass components. The resulting mass model fits are shown in Table 3 and Fig. 11. All three dark matter halo models result in reasonably good fits. The goodness of fit of the pseudo-isothermal halo model is somewhat lower compared to the Burkert and NFW halo models. The lower performance of the pseudo-isothermal halo is mainly due to its $r^{-2}$ density profile at large radii. As a consequence, the velocity curve will continue to increase and eventually converge to a parameter-dependent constant, $v_{esc}$. Therefore, the pseudo-isothermal halo model cannot explain the decreasing rotation curve of NGC 300, whereas the Burkert and NFW halo models (both with an $r^{-3}$ behaviour) are doing better. Of course, all three halo models produce a lower reduced $\chi^2$ in the case of free stellar and gas mass scaling factors. Whereas for the pseudo-isothermal and NFW haloes the improvement is significant, the Burkert halo is the only model to produce a good fit with fixed mass scaling factors. In the case of free mass scaling factors, we obtain values in the range of $f_\star \approx 1$ to 3 and $f_{gas} \approx 3$ to 5. Fixing the gas mass scaling factor to $f_{gas} = 1$ yields somewhat smaller stellar mass scaling factors of $f_\star \approx 1.6$ to 2.2.

As the stellar mass scaling factor strongly depends on the assumptions made about the stellar mass-to-light ratio of NGC 300, a higher value of $f_\star$ can arise from differences in star formation history or metallicity compared to the standard spiral galaxy model found by Bell & de Jong (2001). In comparison, the best mass model fit for NGC 300 found by Kent (1987) yields $f_\star = 1.0$ (relative to our stellar disc mass mass of $1.0 \times 10^{10}$ M$_{\odot}$), and his maximum-disc model has $f_\star = 3.1$. Puche et al. (1990) derive somewhat larger values of $f_\star = 2.2$ and 4.3 for their best-fitting and maximum-disc models, respectively. These numbers are all in general agreement, but they also expose the uncertainties in the determination of the stellar mass-to-light ratio and the total stellar disc mass of NGC 300.

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3 Note that the fit for the NFW halo with fixed gas mass scaling factor failed, because the best-fitting model resulted in a negative stellar mass scaling factor. Therefore, this case will not be presented and discussed here.
Table 3. Results of the mass modelling of NGC 300 for the pseudo-isothermal (ISO), Burkert and NFW dark matter halo profiles. \( f_\star \) and \( f_{\text{gas}} \) are the mass scaling factors for the stellar and gaseous disc, respectively. The parameters in Columns 4 and 5 are the free model parameters of the different dark matter models as explained in the text. Column 6 lists the reduced \( \chi^2 \) value of the model as a measure of the goodness of fit. The last two columns list the total mass, \( M_{\text{tot}} \), of the model within a radius of \( r = 18.4 \) kpc and the fraction of dark matter, \( f_{\text{DM}} \). Note that the NFW fit with fixed gas mass produced negative stellar masses and is therefore not listed.

| Halo model  | \( f_\star \) | \( f_{\text{gas}} \) | \( r_c \) (kpc) | \( \varrho_0 \) (10\(^\text{10} \) M\(_\odot\) pc\(^{-3}\)) | \( \chi^2_{\text{red}} \) | \( M_{\text{tot}} \) (10\(^\text{10} \) M\(_\odot\)) | \( f_{\text{DM}} \) |
|-------------|----------------|-----------------|----------------|---------------------------------|-----------------|-------------------------------|----------------|
| ISO (fixed) | 1              | 1               | 0.93 ± 0.14   | 0.170 ± 0.046                  | 2.10            | 3.6                           | 0.92           |
| ISO (gas fixed) | 1.6 ± 1.3     | 1               | 1.17 ± 0.61   | 0.107 ± 0.111                  | 2.16            | 3.6                           | 0.90           |
| ISO (free)  | 2.3 ± 0.6      | 4.8 ± 1.0       | 0.74 ± 0.35   | 0.135 ± 0.119                  | 1.17            | 3.3                           | 0.65           |
| Burkert (fixed) | 1             | 1               | 2.78 ± 0.14   | 0.081 ± 0.008                  | 1.18            | 3.2                           | 0.91           |
| Burkert (gas fixed) | 2.2 ± 0.9     | 1               | 3.58 ± 0.75   | 0.044 ± 0.021                  | 1.20            | 3.3                           | 0.88           |
| Burkert (free) | 3.1 ± 0.9      | 3.0 ± 1.4       | 4.04 ± 1.10   | 0.025 ± 0.018                  | 1.12            | 3.3                           | 0.73           |
| NFW (fixed) | 1              | 1               | 5.81 ± 0.56   | 89.7 ± 2.4                     | 1.47            | 3.4                           | 0.91           |
| NFW (free)  | 1.1 ± 1.1      | 3.9 ± 1.0       | 4.00 ± 1.53   | 71.9 ± 6.7                     | 0.95            | 3.3                           | 0.74           |

Figure 11. Results of the fitting of mass models to the rotation curve of NGC 300. The panels show, from top to bottom, the results for the pseudo-isothermal halo, the Burkert halo and the NFW halo. For each halo model the results for fixed, partly fixed (gas only), and free stellar and gaseous mass components are shown. The black data points with error bars show the observed rotation curve. The stellar, gaseous and dark matter components are plotted as the dotted, dashed and solid black lines, respectively. The total velocity profile of the model is plotted as the solid grey line. Note that the NFW fit with fixed gas mass produced negative stellar masses and is therefore not displayed.
The free mass scaling factors for the gaseous component are somewhat higher than expected. A factor of 2 can still be explained by optical depth effects in the inner regions of the gas disc, significant amounts of ionized gas throughout the disc, or missing flux in our H I map due to lack of short interferometer spacings. Gas mass scaling factors of 4 or 5, however, seem unreasonably large and not realistic.

Note that in the very inner region of NGC 300 the value of the rotation velocity of the gas disc is negative (see Fig. 11). This does not imply counter-rotation of the gas or the presence of negative mass, but simply reflects a net outward force on test particles due to the central depression of the gas disc. This net outward force results in a negative value of $v^2_{\text{gas}}$ and therefore an imaginary velocity in the mathematical description of mass models that is usually expressed by negative values of $v^2_{\text{gas}}$.

In addition to the dark matter models discussed above we also fitted two models without any dark matter component at all, using Newtonian dynamics and (non-relativistic) Modified Newtonian Dynamics (MOND; Milgrom 1983), respectively. In both cases, only the stellar and gas mass scaling factors were left as free parameters of the fitting procedure. For the MOND model we assumed a constant $d_0 = 1.21 \times 10^{-19} \text{ m s}^{-2}$ (Begeman et al. 1991).4 The resulting mass models are shown in Table 4 and Fig. 12.

Table 4. Results of the mass modelling of NGC 300 for Newtonian dynamics and MOND under the assumption of no additional dark matter halo. $f_\star$ and $f_{\text{gas}}$ are the mass scaling factors for the stellar and gaseous disc, respectively. The last column lists the reduced $\chi^2$ value of the model as a measure for the goodness of fit.

| Dynamics          | $f_\star$   | $f_{\text{gas}}$ | $\chi^2_{\text{red}}$ |
|-------------------|-------------|------------------|-----------------------|
| Newtonian (gas fixed)   | 9.5 ± 1.4  | 1                | 67.42                 |
| Newtonian (free)        | 4.2 ± 0.3  | 8.4 ± 0.3       | 2.17                  |
| MOND (gas fixed)        | 2.2 ± 0.2  | 1                | 3.31                  |
| MOND (free)             | 2.6 ± 0.2  | 0.6 ± 0.2       | 2.50                  |

Neither of the two models produces meaningful results. The best fit in the MOND scenario ($\chi^2_{\text{red}} = 2.50$) yields mass scaling factors of $f_\star = 2.6 ± 0.2$ and $f_{\text{gas}} = 0.6 ± 0.2$ for the stellar and gaseous disc, respectively. Apart from the significantly larger $\chi^2_{\text{red}}$ compared to all of the dark matter models with free mass scaling factors, the MOND model results in a considerable downscaling of the gas disc mass. This is an implausible result because the derived gas mass surface density was directly derived from the observed H I column densities and must therefore be a lower limit. Fixing the mass scaling factor for the gas disc to a value of $f_{\text{gas}} = 1$ slightly reduces the stellar mass scaling factor to $f_\star = 2.2 ± 0.2$, the goodness-of-fit parameter, however, significantly deteriorates to $\chi^2_{\text{red}} = 3.31$.

The reason for the inferior performance of MOND is the decrease in rotation velocity at larger radii. MOND has been designed to explain the flat rotation curves at large radii. MOND has been designed to explain the flat rotation curves at large radii. MOND has been designed to explain the flat rotation curves at large radii. MOND has been designed to explain the flat rotation curves at large radii. MOND has been designed to explain the flat rotation curves at large radii.

5 DISCUSSION

5.1 Origin of the outer disc

A conspicuous feature of NGC 300 is its extended outer H I disc spanning more than 1° (equivalent to about 35 kpc) across the sky. Although the outer disc was partly mapped by previous observations (e.g. Puche et al. 1990), this is the first time that its extent has been imaged out to the $10^{19} \text{ cm}^{-2}$ column density level with moderately high spatial resolution of approximately 1 kpc. The results of our tilted ring model suggest that there is a substantial change in position angle between the inner and outer disc, resulting in a twisted appearance of NGC 300 which is particularly obvious in the velocity field.

One possible scenario for this twist is that the distortion and warping of the outer disc of NGC 300 were caused by tidal forces during a recent encounter with another galaxy. A potential candidate for a close encounter could be NGC 55. Both galaxies are separated by about 8° on the sky, corresponding to a projected separation of about 270 kpc.5 Under the assumption that both galaxies move away from each other at a relative velocity of 200 km s$^{-1}$, there would have been a close encounter between NGC 55 and NGC 300 is its extended outer H I disc spanning more than 1° (equivalent to about 35 kpc) across the sky. Although the outer disc was partly mapped by previous observations (e.g. Puche et al. 1990), this is the first time that its extent has been imaged out to the $10^{19} \text{ cm}^{-2}$ column density level with moderately high spatial resolution of approximately 1 kpc. The results of our tilted ring model suggest that there is a substantial change in position angle between the inner and outer disc, resulting in a twisted appearance of NGC 300 which is particularly obvious in the velocity field.

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4 Fits with variable $d_0$ and fixed mass scaling factors resulted in very similar values of $d_0 \approx 1.3 \times 10^{-19} \text{ m s}^{-2}$.

5 NGC 55 has approximately the same distance from the Milky Way as NGC 300 (Pietrzynski et al. 2006).
300 about 1.3 gigayears (Ga) ago. This time-scale is comparable to the 1.5 Ga that have passed since the previous perigalactic passage of the Magellanic Clouds on their orbit about the Milky Way and the resulting creation of the Magellanic Stream as predicted by numerical simulations (Gardiner & Noguchi 1996; Yoshizawa & Noguchi 2003; however see Mastropietro 2009).

Alternatively, the distortion of the H I disc of NGC 300 could have been caused by a recent encounter with a smaller companion galaxy. The nearest currently known companion is the dwarf-spheroidal galaxy ESO 294−G010. Its distance of about 1.9 Mpc (Karachentsev et al. 2003) is the same as that of NGC 55 and NGC 300, and its angular separation from NGC 300 is 6.9, equivalent to a physical separation of about 230 kpc. Its small size (Bouchard et al. 2005) and relatively large separation from NGC 300, however, suggest that ESO 294−G010 has never had any significant gravitational influence on NGC 300. At the same time, ESO 294−G010 is much closer to NGC 55 with an angular separation of only 3.5 equivalent to about 115 kpc.

Deep optical observations of two fields in the outer part of NGC 300 with the Gemini South 8-m telescope by Bland-Hawthorn et al. (2005) revealed an extended stellar disc reaching out to a radius of at least 24 arcmin (equivalent to about 14 kpc or 10 optical scale-lengths). Surprisingly, the luminosity of the stellar disc of NGC 300 shows a simple exponential profile over its entire radial extent (except for the nuclear region) without any indication of a deviation or break. This seems to contradict our observation of a strongly warped H I disc with a rather discontinuous transition between the inner and outer disc. If this warp were the result of tidal interaction, the stellar disc should have been affected in the same way.

It is important to note that Bland-Hawthorn et al. (2005) did not map the entire two-dimensional distribution of the outer disc on the sky, but observed only two fields in the south-eastern quadrant of NGC 300. Any warp in the stellar disc would therefore have to affect the stars at this particular azimuthal angle to be discernible, and further optical imaging at different azimuthal angles would be required to firmly exclude the presence of a warp in the outer stellar disc.

Bland-Hawthorn et al. (2005) discuss some of the implications of this discrepancy and speculate about the origin of the extended stellar disc, including the possibility of stars being scattered from the inner disc. Another possibility is that gas accreted by NGC 300 through hot or cold accretion modes could have fuelled low levels of star formation in the outer disc. In this case, however, there should be a break in the radial stellar surface brightness profile.

Alternatively, stars could have formed in the outer H I disc as a result of instabilities such as spiral density waves. In order to test this hypothesis, Bland-Hawthorn et al. (2005) calculated the Toomre Q parameter,

$$ Q(r) = \frac{\sigma(r)\kappa(r)}{3.36 G \Sigma_{\text{gas}}(r)} $$

(Toomre 1964), based on the H I data of Puche et al. (1990). Here, $\sigma(r)$ is the velocity dispersion of the gas disc, $\kappa(r)$ is the epicyclic frequency of the rotating disc defined by

$$ \kappa^2 = \frac{\partial^2}{\partial r^2} \left( \frac{v^2}{r^2} + \frac{v \, dv}{r \, dr} \right) $$

and $\Sigma_{\text{gas}}(r)$ denotes the gas mass surface density, all three of which are a function of galactocentric radius, $r$. Bland-Hawthorn et al. (2005) found values in excess of $Q \approx 5$ for the disc beyond a radius of 10 arcmin (equivalent to about 5.5 kpc), suggesting that the outer disc of NGC 300 is stable with respect to axisymmetric instabilities.

Figure 12. Same as in Fig. 11, but for non-relativistic MOND (top) and Newtonian dynamics (bottom). In both cases, no additional dark matter was included. In the left-hand column the gaseous mass component was held fixed whereas the stellar component was allowed to vary. In the right-hand column both components were variable.
Recalculation of $Q$ based on our H\textsc{i} observations with the ATCA, however, suggests somewhat smaller $Q$ parameters over much of the disc of NGC 300. Using equation (22) and assuming the same constant gas velocity dispersion of $\sigma = 5$ km s$^{-1}$ as Bland-Hawthorn et al. (2005) yield typical values of $Q \approx 1$ to 3 between 2 and 12 kpc radius (Fig. 13), suggesting that the gas disc may be susceptible to axisymmetric instabilities. However, a slightly higher and more realistic velocity dispersion of 10 km s$^{-1}$ (Tamburro et al. 2009) would result in the disc being Toomre stable at most radii. Furthermore, recent studies suggest that the star formation efficiency in disc galaxies is regulated by other effects, such as the physics of the ISM on small scales (Leroy et al. 2008) or the gas pressure in the disc (Blitz & Rosolowsky 2006), and that the Toomre $Q$ parameter does not necessarily provide an accurate description of the ability of the disc to form stars.

Obviously, the next logical step in our attempt to understand the evolutionary history of NGC 300 would be a more detailed study of the outer stellar disc to determine the age and chemical composition of the stars. This was recently achieved by Vlajić, Bland-Hawthorn & Freeman (2009) through $g'$ and $i'$ photometry of three fields in the outskirts of NGC 300 with the Gemini South telescope. The observations confirmed that the stellar population in the outer disc is predominantly old. At the same time, there appears to be a radial gradient in metallicity with a sudden break at a radius of about 10 kpc. While the inner disc shows a radially decreasing metallicity, this trend surprisingly reverses in the outer disc. Interestingly, the break occurs near the boundary between the inner and outer H\textsc{i} disc of NGC 300, although it is not clear at this point whether this is just a coincidence or whether there is a physical connection between the two phenomena.

Vlajić et al. (2009) propose two possible scenarios for the observed break in the metallicity gradient. Either there could have been some kind of radial mixing of stars in the disc or star formation could have slowed down and been less active during the evolution of NGC 300, resulting in a moderate metallicity gradient in the inner disc, but an almost flat and pristine metallicity distribution across the outer disc. In both cases, the gas in the outer disc would not play any significant role in the recent star formation activity of NGC 300, which is consistent with the generally old age ($\approx 1$ Ga) of the stellar population in the outer disc and the presence of only a small fraction of younger (a few hundred million years) main-sequence stars.

\section{5.2 Ram-pressure interaction}

The aforementioned strong asymmetries found in the outer H\textsc{i} disc of NGC 300 are suggestive of ram-pressure interaction with the surrounding intergalactic medium (IGM) of the Sculptor group. As NGC 300 is moving through the IGM, gas at the leading edge of the disc would be compressed, whereas gas at the trailing edge of the disc would be dragged and stripped by ram-pressure forces (see e.g. Vollmer 2009 and references therein). The influence of ram pressure has been mainly observed in the dense IGM of massive galaxy clusters (e.g. White et al. 1991; Vollmer et al. 2004), in particular the nearby Virgo cluster (Giovanelli & Haynes 1983), where ram pressure is believed to be responsible for the stripping and removal of gas from galaxies (Vollmer et al. 2001). In contrast, only very few cases of ram-pressure stripping in galaxy groups have been reported so far (e.g. Kantharia et al. 2005; McConnachie et al. 2007; Bouchard et al. 2007).

To assess whether ram pressure could have caused the observed asymmetries in the gas disc of NGC 300 we can compare the expected ram-pressure forces with the gravitational forces stabilizing the disc. The pressure imposed on the gas disc by a galaxy’s own gravitational potential can be expressed as

$$P_{\text{grav}} = \Sigma_{\text{gas}}(r) \left| \frac{\partial \Phi(r)}{\partial z} \right|_{\text{max}}$$

(Gunn & Gott 1972; Roediger & Hensler 2005). Here, $\Sigma_{\text{gas}}(r)$ is the gas mass surface density of the disc as a function of radius, and $\Phi(r)$ denotes the gravitational potential of the disc. The term on the right-hand side of equation (24) determines the maximum of the absolute value of the gravitational acceleration perpendicular to the disc, with $z$ being the height above the disc.

The gas disc will be subject to ram-pressure stripping if the pressure exerted by the IGM exceeds the stabilizing gravitational pressure as determined by equation (24). The ram pressure of the IGM is determined by the density of the IGM, $\rho_{\text{IGM}}$, and the relative velocity of the galaxy with respect to the surrounding medium, $v_{\text{rel}}$, thus

$$P_{\text{ram}} = \rho_{\text{IGM}} v_{\text{rel}}^2.$$  \hspace{1cm} (25)

Ram-pressure stripping of gas in the disc will occur whenever the instability condition $P_{\text{ram}} > P_{\text{grav}}$ is fulfilled. As the gravitational pressure will be a strong function of galactocentric radius, one can also define a truncation radius at which ram-pressure forces start to dominate over gravity. The simple analytic approach described above assumes that the galaxy is moving face-on through the IGM, however, hydrodynamical simulations have demonstrated that even for larger inclination angles of the disc of up to about 60$^\circ$ with respect to the direction of motion the analytic approach produces meaningful results (Roediger & Brüggen 2006).

In order to assess the stability of the gas disc of NGC 300 against ram-pressure stripping we have calculated the instability condition for different scenarios. We assumed the gravitational potential of the galaxy to be dominated by its dark matter halo and neglected the potential of the stellar disc and gas disc. This assumption will be met at greater heights, $z$, above the disc plane in the outermost regions of the disc where we expect the gas to be particularly vulnerable to ram-pressure stripping. Furthermore, we assumed the dark matter halo to have an NFW profile with the parameters (for the model with fixed stellar and gaseous mass scaling factors) derived in Section 4.4 and listed in Table 3. The gravitational potential of the NFW

\begin{figure}[h]
\centering
\includegraphics[width=0.5\textwidth]{figure13.png}
\caption{Toomre $Q$ parameter of the gas disc of NGC 300 as a function of galactocentric radius.}
\end{figure}
Figure 14. Ratio between gravitational pressure and ram pressure in the disc of NGC 300 as a function of radius. The left-hand panel shows the pressure ratio for a constant velocity of $v_{\text{rel}} = 200 \text{ km s}^{-1}$ and five different densities of (from top to bottom) $n_{\text{IGM}} = 5 \times 10^{-6}$, $1 \times 10^{-5}$, $2 \times 10^{-5}$, $5 \times 10^{-5}$ and $1 \times 10^{-4} \text{ cm}^{-3}$. The right-hand panel shows the pressure ratio for a constant density of $n_{\text{IGM}} = 5 \times 10^{-5} \text{ cm}^{-3}$ and five different velocities of (from top to bottom) $v_{\text{rel}} = 100$, 150, 200, 250 and 300 km s$^{-1}$. The region above the horizontal black line at $\log_{10}(P_{\text{grav}}/P_{\text{ram}}) = 0$ is dominated by gravity, and the gas disc is stable. The region below that line is dominated by ram pressure, and the gas will be subject to ram-pressure stripping.

Figure 15. Left: schematic overview of the gravitational acceleration, $a_z$, of the NFW halo perpendicular to the disc as a function of height, $z$, above the plane. At $z = z_{\text{eq}}$, gravitational pressure and ram pressure are in balance. Right: height, $z_{\text{eq}}$, above the disc plane of NGC 300 where equilibrium between gravitational pressure and ram pressure is achieved. The situation for two different IGM densities of $n_{\text{IGM}} = 10^{-5}$ and $10^{-4} \text{ cm}^{-3}$ is shown under the assumption of face-on motion and a relative velocity of NGC 300 with respect to the surrounding IGM of $v_{\text{rel}} = 150 \text{ km s}^{-1}$.

The gravitational acceleration, $a_z$, of the NFW halo perpendicular to the disc as a function of height, $z$, above the plane is given by

$$a_z = \frac{GM_{200} \ln \left(1 + \frac{r}{r_s}\right)}{r \left[\ln(1 + c) - \frac{1}{1+c}\right]}$$

(Hayashi, Navarro & Springel 2007) where $M_{200}$, $r_s$ and $c$ are parameters of the NFW profile as discussed in Section 4.3.3. Solving equation (24) for the NFW potential and combining it with equation (25) allow us to investigate the instability condition for different values of the IGM density and relative velocity of NGC 300. The results are presented in Fig. 14.

The left-hand panel of Fig. 14 shows the situation for a constant velocity of $v_{\text{rel}} = 200 \text{ km s}^{-1}$ of NGC 300 with respect to the IGM but for five different IGM densities. The right-hand panel of Fig. 14 shows the situation for a constant IGM density of $n_{\text{IGM}} = 5 \times 10^{-5} \text{ cm}^{-3}$ but for five different velocities. As we would expect, most of the gas disc of NGC 300 is many orders of magnitude above the instability condition of $\log_{10}(P_{\text{grav}}/P_{\text{ram}}) < 0$ represented by the horizontal black line. However, under certain conditions the outermost part of the gas disc beyond a radius of about 15 kpc will get near or just below the instability line, in particular for IGM densities in excess of about a few times $10^{-5} \text{ cm}^{-3}$ and sufficiently high relative velocities of $v_{\text{rel}} \gtrsim 200 \text{ km s}^{-1}$. The density values assumed here are consistent with constraints on the density of the Local Group medium by various studies (e.g. Rasmussen & Pedersen 2001; Sembach et al. 2003; Williams et al. 2005).

It is interesting to note that the outer edge of the H$\text{I}$ disc of NGC 300 appears to be close to balance between gravitational and ram-pressure forces over a range of reasonable values for density and velocity. This could indicate that the edge of the disc is defined by the aforementioned truncation radius at which ram-pressure forces start to dominate over gravity. A stable disc configuration beyond that radius would be impossible, suggesting that under certain conditions ram pressure could in general be responsible for establishing the outer edge of H$\text{I}$ discs of galaxies in group environments.

Furthermore, ram pressure could also result in a significant vertical displacement of disc gas and thereby contribute to the warping observed in the outer disc of many spiral galaxies. This situation is shown schematically in the left-hand panel of Fig. 15 where the gravitational acceleration, $a_z$, of the NFW halo perpendicular to the gas disc is shown as a function of height, $z$, above the disc plane. Under the assumption of a face-on wind caused by the surrounding IGM, there will be for each galactocentric radius an equilibrium pressure and sufficiently high relative velocities of $v_{\text{rel}} \gtrsim 200 \text{ km s}^{-1}$. The density values assumed here are consistent with constraints on the density of the Local Group medium by various studies (e.g. Rasmussen & Pedersen 2001; Sembach et al. 2003; Williams et al. 2005).

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height, \( z_{eq} \), at which the gravitational pressure in the disc will be in balance with the ram pressure of the wind. Of course, there will be no such equilibrium for radii greater than the truncation radius beyond which the ram pressure always exceeds the gravitational pressure at any height above the disc.

The right-hand panel of Fig. 15 shows the expected value of \( z_{eq} \) as a function of galactocentric radius in NGC 300 for two different IGM densities of \( \rho_{IGM} = 10^{-5} \) and \( 10^{-4} \) cm\(^{-3} \) and under the assumption of a constant relative velocity of \( v_{rel} = 150 \) km s\(^{-1} \). Over much of the disc of NGC 300 the expected equilibrium height, and thus vertical displacement, of the gas is very small. Towards the outer disc the equilibrium height exceeds 1 kpc with a maximum value of \( z_{eq} \approx 1.6 \) kpc in the outermost radial bin under the assumption of \( \rho_{IGM} = 10^{-5} \) cm\(^{-3} \). If we increase the IGM density by a factor of 10 to \( 10^{-4} \) cm\(^{-3} \) the equilibrium height increases to almost 10 kpc at \( r = 16.6 \) kpc, and beyond that radius there is no solution at all because we would exceed the truncation radius. These estimates illustrate that ram pressure may have an impact on the vertical structure of the H\(_I\) of NGC 300 depending on the properties of the surrounding IGM. We can also rule out higher IGM densities of well above \( 10^{-5} \) cm\(^{-3} \) as they would result in a destruction of the outer parts of the observed H\(_I\) disc.

Also note that in all our calculations we neglected the gravitational potential of the stellar and gaseous discs, hence underestimating the restoring force. This will particularly be the case for the inner disc of NGC 300 and locations close to the disc plane, where the ratio between gravitational pressure and ram pressure will be significantly higher than indicated in Fig. 14. Near the outer edge of the H\(_I\) disc, however, the contribution from stars and gas to the gravitational potential is much smaller compared to the dark matter component. While the stellar mass surface density across the outer disc is immeasurably small, the contribution of the gas disc to the gravitational potential is comparable to that of the dark matter halo within a few hundred pc of the disc plane and negligible for \( z \gtrsim 1 \) kpc. Therefore, our general conclusions about the stability of the outer disc are not affected by the additional contribution from the gas, and our numerical results near the outer edge of the disc are accurate within a factor of about 2 to 3.

Our results suggest that the edge of the gas disc of NGC 300 may indeed be subject to ram-pressure stripping, although the effect will likely be subtle. This result is consistent with our H\(_I\) observations which show notable asymmetries between the north-western and south-eastern part of NGC 300 and signs of distortion along the north-western edge of the H\(_I\) disc. In this scenario the proper motion of NGC 300 on the sky would be in the south-eastern direction, pointing away from NGC 55.

The ram-pressure scenario is also consistent with the offsets between the H\(_I\) gas and the stellar distribution found in several dwarf galaxies of the Sculptor group by Bouchard et al. (2005).\(^6\) Although these effects are by far not as strong as in massive galaxy clusters, our results suggest that even in modest-sized galaxies ram-pressure interaction does play a role in shaping the faint, outer gas discs of spiral galaxies in a density regime often not exposed by shallow H\(_I\) observations. This finding once more highlights the need for deep and large-scale imaging of galaxies in the 21-cm line of H\(_I\) in order to understand the role of interaction and feedback between galaxies and the IGM.

5.3 Gas accretion

Alternatively, some of the observed asymmetries in the H\(_I\) disc of NGC 300 could be the result of cold-mode accretion flows of primordial gas. Lopsidedness of the stellar and gaseous discs of galaxies is a well-known and common phenomenon (e.g. Baldwin, Lynden-Bell & Sancisi 1980; Richter & Sancisi 1994; Rix & Zaritsky 1995; Haynes et al. 1998). Among other processes (Jog & Combes 2009), cold-mode accretion flows of primordial gas have been discussed as the potential origin of the observed asymmetries (Bournaud et al. 2005; Sancisi et al. 2008).

Hydrodynamical simulations by Kereš et al. (2005) have shown that there are two distinct modes of gas accretion on to galaxies: hot-mode accretion of shock-heated gas at temperatures in excess of the virial temperature of the dark matter halo, \( T > T_{vir} \approx 10^5 \) to \( 10^7 \) K, and cold-mode accretion of gas at lower temperatures of \( T < T_{vir} \). While in their simulations the cold mode dominates accretion at higher redshifts, the hot mode becomes increasingly more important at lower redshifts, as many dark matter haloes exceed a critical virial mass of about \( 10^{11.3-12} \) M\(_\odot\) above which accreted gas becomes predominantly shock-heated (Kereš et al. 2005, 2009; Dekel & Birnboim 2006). Furthermore, cold-mode accretion is geometrically different from hot-mode accretion in that it occurs along filaments and therefore is not radially symmetric.

Asymmetric cold-mode accretion could have resulted in asymmetries in the outer gas disc of NGC 300, because the accreted gas would end up in non-circular orbits with substantial orbital timescales in excess of about 1 Ga near the outer edge of the gas disc. This scenario is supported by numerical simulations of Bournaud et al. (2005) who conclude that accretion along filaments of the cosmic web with accretion rates of a few M\(_\odot\) yr\(^{-1}\) is likely to be responsible for the ubiquity of lopsidedness observed in the stellar and gaseous discs of galaxies.

We conclude that sensitive H\(_I\) observations of a large sample of galaxies would provide the opportunity to systematically study the kinematics of gas in the outer disc to determine the contribution of external processes such as ram pressure or gas accretion.

6 SUMMARY

We have used the ATCA to map a large area of about \( 2^\circ \times 2^\circ \) (corresponding to a projected size of about \( 65 \times 65 \) kpc\(^2\)) around the Sculptor group galaxy NGC 300 in the 21-cm line of H\(_I\). We achieved a 5\( \sigma \) H\(_I\) column density sensitivity of \( 1.0 \times 10^{15} \) cm\(^{-2} \) over \( 8 \) km s\(^{-1} \) for emission filling the synthesized beam of 180\( \times \) 88 arcsec\(^2\) FWHM. The corresponding 5\( \sigma \) H\(_I\) mass sensitivity is \( 1.2 \times 10^9 \) M\(_\odot\) under the assumption of a distance of 1.9 Mpc for NGC 300.

The major results and conclusions from our analysis of the H\(_I\) emission in NGC 300 are as follows.

(i) NGC 300 is characterized by a dense inner disc with column densities in excess of \( 5 \times 10^{20} \) cm\(^{-2} \) and an extended outer disc with column densities of typically less than \( 2 \times 10^{20} \) cm\(^{-2} \). The inner disc has an orientation angle of 290\(^\circ\) and is perfectly aligned with the optical (stellar) disc. The outer disc has a totally different orientation angle of 332\(^\circ\), and its major axis spans more than 1\(^\circ\) on the sky equivalent to a linear diameter of about 35 kpc within the \( 10^{20} \) cm\(^{-2} \) column density contour.

(ii) Under the assumption that the gas is optically thin we derive a total H\(_I\) mass for NGC 300 of \( 1.5 \times 10^9 \) M\(_\odot\). This is only slightly short of the single-dish value of \( 1.7 \times 10^9 \) M\(_\odot\) found by Koribalski

\(^6\) It should be noted, though, that their ATCA detections are of low significance, resulting in large uncertainties in the position of the H\(_I\) emission.
indicating that the ATCA recovered about 90 per cent of the total flux. Of the total H\textsc{i} mass of NGC 300, about 8.5 \times 10^8 M_\odot (or 57 per cent) is contributed by the inner disc and 6.5 \times 10^8 M_\odot (or 43 per cent) by the outer disc.

(iii) We fitted a tilted ring model to the velocity field of NGC 300 to determine the H\textsc{i} rotation curve out to a radius of 18.4 kpc. The derived rotation curve rises out to a radius of approximately 10 kpc where we observe a maximum velocity of about 100 km s\textsuperscript{-1}. Further out the rotation curve slowly decreases to about 83 km s\textsuperscript{-1} in the outermost ring at 18.4 kpc radius.

(iv) We constructed different mass models of NGC 300 involving a stellar disc, a gas disc and a dark matter halo. We obtain good fits for both the Burkert and NFW dark matter halo models, both of which successfully cope with the decreasing rotation velocity in the outer parts of the galaxy. Fits with either Newtonian dynamics or MOND and no dark matter halo at all result in much higher \chi\textsuperscript{2} values and unrealistic mass scaling factors for the gaseous disc.

(v) The twisted structure of the H\textsc{i} disc of NGC 300 suggests distortion by tidal interaction, but no nearby companion galaxy is currently known that could have exerted strong tidal forces on the disc. At the same time, optical studies by Bland-Hawthorn et al. (2001) provide evidence against tidal interaction by demonstrating that the stellar disc of NGC 300 has a simple exponential radial profile out to the largest detected radii without any sign of distortion.

(vi) Optical observations by Vlaji\c{c} et al. (2009) have shown that the stellar population in the outer disc is predominantly old (>1 Ga) and that therefore the outer gas disc does not currently play a significant role in the star formation activity of NGC 300.

(vii) Asymmetries in the outer H\textsc{i} disc suggest that NGC 300 is affected by ram-pressure interaction while moving through the IGM of the Sculptor group, with its proper motion on the sky directed approximately to the south-east. Estimates show that, under reasonable assumptions on the IGM density and relative velocity, the outer edge of the H\textsc{i} disc of NGC 300 may be significantly distorted by ram pressure. From our analysis we conclude that the density of the IGM in the Sculptor group must be lower than about 10\textsuperscript{-5} cm\textsuperscript{-3} as otherwise the outer parts of the H\textsc{i} disc of NGC 300 could not have survived.

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