Keck Spectroscopy of the Coma Cluster Ultra-Diffuse Galaxy Y358: Dynamical Mass in a Wider Context

Jonah S. Gannon, Duncan A. Forbes, Jean P. Brodie, Aaron J. Romanowsky, Warrick J. Couch and Anna Ferré-Mateu

1 Centre for Astrophysics and Supercomputing, Swinburne University, John Street, Hawthorn VIC 3122, Australia
2 Department of Physics and Astronomy, San José State University, One Washington Square, San Jose, CA 95192, USA
3 Department of Physics and Astronomy, Brown University, 17 Hope St, Providence, RI 02912, USA
4 Instituto de Astrofísica de Canarias, Calle Vía Láctea S/N, E-38205, La Laguna, Tenerife, Spain
5 Departamento de Astrofísica, Universidad de La Laguna, 38206, La Laguna (S.C. Tenerife), Spain

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ABSTRACT

We examine ultra-diffuse galaxies (UDGs) and their relation to non-UDGs in mass–radius–luminosity space. We begin by publishing Keck/KCWI spectroscopy for the Coma cluster UDG Y358, for which we measure both a recessional velocity and velocity dispersion. Our recessional velocity confirms association with the Coma cluster and Y358’s status as a UDG. From our velocity dispersion (19 ± 3 km s⁻¹) we calculate a dynamical mass within the half-light radius which provides evidence for a core in Y358’s dark matter halo. We compare this dynamical mass, along with those for globular cluster (GC)-rich/-poor UDGs in the literature, to mass profiles for isolated, gas-rich UDGs and UDGs in the NIHAO/FIRE simulations. We find GC-poor UDGs have dynamical masses similar to isolated, gas-rich UDGs, suggesting an evolutionary pathway may exist between the two. Conversely, GC-rich UDGs have dynamical masses too massive to be easily explained as the evolution of the isolated, gas-rich UDGs. The simulated UDGs match the dynamical masses of the GC-rich UDGs. However, once compared in stellar mass – halo mass space, the FIRE/NIHAO simulated UDGs do not match the halo masses of either the isolated, gas-rich UDGs or the GC-rich UDGs at the same stellar mass. Finally, we supplement our data for Y358 with other UDGs that have measured velocity dispersions in the literature. We compare this sample to a wide range of non-UDGs in mass–radius–luminosity space, finding UDGs have a similar locus to non-UDGs of similar luminosity with the primary difference being their larger half-light radii.

Key words: galaxies: fundamental parameters – galaxies: kinematics and dynamics – galaxies: formation – galaxies: elliptical and lenticular – galaxies: halos

1 INTRODUCTION

The class of “ultra-diffuse galaxy” (UDG) was first coined by van Dokkum et al. (2015) in relation to a subset of large half-light radius, low surface brightness galaxies in the Coma cluster. Formally, they classified UDGs as galaxies with half-light radius, \( R_e > 1.5 \) kpc; and central surface brightness, \( \mu_0, e > 24 \) mag arcsec⁻². Galaxies fitting this definition have been discovered in a wide range of environments both before (e.g., Disney 1976; Sandage & Binggeli 1984; Bothun et al. 1987; Impey et al. 1988; Impey & Bothun 1997; Dalcanton et al. 1997) and after 2015 (e.g., Yagi et al. 2016; Martínez-Delgado et al. 2016; van der Burg et al. 2017; Román & Trujillo 2017b,a; Román et al. 2019; Janssens et al. 2017, 2019; Müller et al. 2018; Prole et al. 2019b; Forbes et al. 2019, 2020b; Zaritsky et al. 2019, 2021; Barbosa et al. 2020).

It is worth noting that since their coining by van Dokkum et al. (2015), many other authors have applied the same UDG term to galaxies fitting a different criteria set. For example, in the catalogue of Yagi et al. (2016) the UDG size criterion was relaxed to \( R_e > 0.7 \) kpc. Other authors have used a surface brightness criterion based on the average surface brightness within the half-light radius (\( \langle \mu_e \rangle \); e.g., van der Burg et al. 2017; Janssens et al. 2017, 2019; Gannon et al. 2022), or altered the surface brightness/filter band at which it applies (e.g., Janssens et al. 2017, 2019; Forbes et al. 2020b). The studies of Ruiz-Lara et al. (2018) and Chilingarian et al. (2019) went further, applying the UDG term to a set of galaxies that are generally brighter and smaller than the original definition. Using the ROMULUS simulations, Van Nest et al. (2022) found that the choice of UDG criteria is key, having a large impact on the implied mechanisms underpinning their formation. Specifically, definitions for what comprises a ‘UDG’ that are less restrictive may dilute the link between objects fitting the definition and their underlying formation mechanism.

For UDGs, their necessarily faint nature means spectroscopy of their stellar body requires a large time investment on 8m+ class telescopes. While gas-rich UDGs can be studied using their gas-kinematics (e.g., Mancera Piña et al. 2019, 2022; Kong et al. 2022)
this method is largely available for quiescent UDGs. As such, spectroscopy has largely focused on deriving the properties of single, or a small handful of, UDGs (e.g., van Dokkum et al. 2017; Toloba et al. 2018; Alabi et al. 2018; Ferré-Mateu et al. 2018; Martín-Navarro et al. 2019; Emsellem et al. 2019; Danieli et al. 2019; van Dokkum et al. 2019; Müller et al. 2020; Gannon et al. 2020, 2021, 2022; Forbes et al. 2021). Many of these UDGs have been targeted because of their extreme properties, even within the UDG class. For example many UDGs have received targeted spectroscopy due to their anomalously populous globular cluster (GC) systems (e.g., Dragonfly 44 and DFXI van Dokkum et al. 2017, 2019), a known indicator of a massive dark matter halo (Spitler & Forbes 2009; Harris et al. 2017; Forbes et al. 2018; Burkert & Forbes 2020; Zaritsky et al. 2022). While this has led to a slew of interesting discoveries, it has likely resulted in an overall literature that is poorly representative of the UDG population as a whole.

Simulations of galaxy formation primarily propose that UDGs form in a ‘puffy dwarf’ scenario. In brief, they suggest UDGs are simply an extension of the regular dwarf galaxy population to larger sizes. The primary cause of this puffing up is usually attributed to higher than average halo spin (Amorisco & Loeb 2016; Rong et al. 2017; Liao et al. 2019), strong stellar feedback (Di Cintio et al. 2017; Chan et al. 2018), tidal forces/quenching (Carleton et al. 2019; Sales et al. 2020; Tremmel et al. 2020), early mergers (Wright et al. 2021) or combinations of the aforementioned four (Jiang et al. 2019; Martin et al. 2019; Liao et al. 2019). It seems likely that these scenarios account for many, perhaps even most, galaxies residing in the UDG definition.

Early work incorporating GCs into simulations of ‘puffy dwarf’ UDG formation suggested the formation of GC-rich UDGs may be possible in dwarf-like dark matter halos (Carleton et al. 2021). However, this formation scenario cannot explain known GC–dark matter halo mass scaling relations and is unable to produce GC-rich UDGs in massive dark matter halos (Gannon et al. 2022).

Alternatively, it has been suggested that GC-rich, massive halo UDGs may be the dark matter dominated remnants of the earliest phases of galaxy formation. The observational expectation is for the galaxy to have quenched early and catastrophically. In doing so it fails to form a large portion of its expected stellar mass (van Dokkum et al. 2016; Peng & Lim 2016; Villaume et al. 2022; Danieli et al. 2022; Janssens et al. 2022; Buzzo et al. 2022). These massive halo UDGs are not reproduced by leading cosmological simulations of galaxy formation. We note the work of Saifollahi et al. (2021, 2022) which suggested the rich GC systems of 5 previously studied Coma cluster UDGs may be the result of measurement error. However even after their measurement corrections, Saifollahi et al. (2022) concluded an early formation and quenching scenario is still one of the most viable formation pathways. Saifollahi et al. (2022) referred to this UDG formation process as a ‘failed dwarf galaxy’ scenario. Furthermore, follow-up spectroscopy, which allows measurement of a dynamical mass, largely supports the idea that GC-rich UDGs may reside in massive dark matter halos (van Dokkum et al. 2019; Gannon et al. 2020; Forbes et al. 2021; Gannon et al. 2022). It is not currently clear what fraction of the population massive halo UDGs represent.

For pressure-supported systems it has been well established that in velocity dispersion, effective radius and surface brightness space, galaxies reside on a so-called “fundamental plane” (Djorgovski & Davis 1987; Faber et al. 1987; Dressler 1987). The fundamental plane offers unique insights into the physical processes generating pressure-supported systems and thus constrains their formation (e.g., Borriello et al. 2003; Cappellari et al. 2006; Forbes et al. 2008; Graves & Faber 2010; Tollerud et al. 2011; Zaritsky et al. 2019).

The fundamental plane and altered forms of it, such as mass–radius–luminosity space (Tollerud et al. 2011) or the fundamental manifold (Zaritsky et al. 2006), have been shown to extend over nearly eight orders of magnitude in luminosity. These offer a connection from the dwarf spheroidals to giant elliptical galaxies (Zaritsky et al. 2006; Forbes et al. 2008; Tollerud et al. 2011). This allows an exploration of the relationship between luminous matter and dark matter halos from the smallest to the largest structures in the Universe. It is also critical to our understanding of the dominant galaxy formation processes on different mass scales. With detailed studies of mass profiles being prohibitively time intensive and still leaving great uncertainty in total UDG halo masses (van Dokkum et al. 2019), placing large samples of UDGs on these relations is key to understanding their formation (cf., Gannon et al. 2022). We adopt the latter approach in this work.

Here we present new Keck II/Keck Cosmic Web Imager (KCWI) spectroscopy for the Coma cluster UDG Y358. From these data we measure both a recessional velocity and a velocity dispersion (Section 2). From our velocity dispersion we measure a dynamical mass. We compare this dynamical mass to dark matter mass profiles to look for evidence of a core or cusp (Section 3). We additionally compare Y358’s dynamical mass, along with dynamical masses for other UDGs, to mass profiles of isolated, gas-rich UDGs along with those from the NIHAO and FIRE simulations (Section 3.2). To contextualise this comparison we compare the UDGs, both observed and simulated, in stellar mass – halo mass space (Section 3.3). We then supplement our Y358 data with those for literature UDGs with the intention of placing all on the fundamental plane (Section 4). In Section 4.1 we discuss the biases present in our sample. In Section 5 we place UDGs in mass–radius–luminosity space, discussing their location on the plane in the context of UDG formation compared to non-UDGs on the plane. We present the concluding remarks of our study in Section 6. The literature sample discussed in Sections 5 & 5 is presented in Appendix A.

2 NEW KECK COSMIC WEB IMAGER DATA

Here we present new KCWI data for the UDG, Y358. We target this galaxy due to its rich GC system which is indicative of a massive dark matter halo. Using the GC counts for Y358 from Lim et al. (2018) (N_{GC} = 28.0 ± 5.3) and the N_{GC} – halo mass relationship of Burkert & Forbes (2020), we infer a total dark matter halo mass of (1.4 ± 0.25) × 10^{11} M_\odot for Y358. The Lim et al. (2018) GC number is between the richness found by van Dokkum et al. (2017, 45±14) and the 90% upper limit from Amorisco et al. (2018, 18.4) for Y358. This is also the number used in the study of Forbes et al. (2020a) for Y358. Based on this GC richness, Y358 is expected to have a dark matter halo > 1 σ more massive than expected given its stellar mass (M_\ast = 1.38 × 10^{8} M_\odot; Forbes et al. 2020a).

The integral field spectroscopy for the UDG Y358 was observed using KCWI (Morrisey et al. 2018) on 2020, March 21st (Program: U191; PI: Brodie). Skies were dark and clear with 1.2” seeing. KCWI was configured using the medium slicer and ‘BH3’ grating with a central wavelength of 5170 Å (R ≈ 9900; σ_{inst} ≈ 13 km s^{-1}). We display a Hubble Space Telescope (HST) image of the galaxy, along with the KCWI pointing in Figure 1.

The data were reduced using the standard KCWI data reduction pipeline along with the extra post-pipeline trimming and flat fielding steps described in Gannon et al. (2020). Spectra were extracted from the reduced data cubes using a 7 by 13 spaxel box centred on the galaxy with offset regions of the slicer as subtracted sky. These spectra were then barycentric corrected (Tollerud 2015) and median
3 RESULTS

We measure a dynamical mass for Y358 within the 3D de-projected half-light radius \( R_{1/2} \) using the mass estimator of Wolf et al. (2010). Using the 2D projected, circularised half-light radius \( R_{e,circ} \) and the luminosity-weighted line-of-sight velocity dispersion within this radius \( \sigma \), it takes the form:

\[
M(< R_{1/2} ) = 930 \left( \frac{\sigma_e^2}{(\text{km s}^{-1})^2} \right) \left( \frac{R_{e,circ}}{\text{pc}} \right) M_\odot \; ;
\]

(1)

where \( R_{1/2} = \frac{4}{3} R_{e,circ} \).

We note this equation requires the luminosity-weighted line-of-sight velocity dispersion within the half-light radius. Our extracted region on Y358 corresponds to a ~ 6.3'' × 6.7'' region which is only slightly smaller than the effective diameter (~ 9''). Our measured velocity dispersion of 19 ± 3 km s\(^{-1}\) should well approximate the required value for Equation 1. We therefore calculate a dynamical mass of 7.1 ± 2.2 × 10\(^8\) M_\odot within 2.8 kpc for Y358 using Equation 1.

3.1 Y358 Halo Mass

In Figure 3 we compare the halo mass estimated from GC counts to the dynamical mass measurement we have obtained using our KCWI data. The comparison of a total halo mass to a mass measurement made within a fixed radius requires the assumption of a dark matter halo profile. Here, we assume a cuspy, NFW (Navarro et al. 1996) halo profile along with a cored, Di Cintio et al. (2014) halo profile. We additionally plot a halo of mass roughly expected for a GC-poor UDG \( (N_{GC} \approx 2; M_{Halo} = 10^{10} M_\odot) \) Burkert & Forbes (2020) for each of the cuspy/cored profiles.

When the profile is forced to be a cuspy NFf profile with normal concentration (i.e., a concentration from Dutton & Macciò 2014) a halo of total mass ~ 6.6 × 10^9 M_\odot is required to have the same enclosed mass as our measurement for Y358. Y358 residing in such a low mass dark matter halo is highly unexpected as it is below the Burkert & Forbes (2020) prediction from its rich GC system (i.e., 1.4 ± 0.25 × 10^{11} M_\odot). There is evidence in the literature that UDGs should obey this relationship (e.g., Gannon et al. 2022) therefore we suggest that Y358 does not reside in a low mass NFW halo. We instead conclude that Y358 likely resides in a cored and/or low concentration halo profile as it must do in order to obey the Burkert & Forbes (2020) relation. Previous works studying UDG dynamical masses have come to similar conclusions for other UDGs (e.g., van Dokkum et al. 2019; Gannon et al. 2022).

3.2 Comparison to Gas-Rich UDGs

Recent work has suggested some isolated, gas-rich field UDGs may reside in low concentration and/or cored dark matter halos (see e.g., Brook et al. 2021; Mancera Piña et al. 2022; Kong et al. 2022). Using resolved HI kinematics for seven such gas-rich isolated UDGs, Kong et al. (2022) were able to fit Read et al. (2016) mass profiles. Their best-fitting parameters are listed in their table 1. Read et al. (2016) mass profiles have the benefit of being able to reproduce observed dark matter cores in the dwarf halo mass regime while providing a convenient fitting function for star/gas kinematics.

We plot these best fitting Read et al. (2016) mass profiles from Kong et al. (2022) for comparison to UDG stellar kinematics in Figure 4. We note that our GC-rich UDGs are primarily in the cluster environment and hence gas poor. The contribution of baryons to their calculated dynamical mass is therefore small (\( \lesssim 10\% \)) and they are extremely dark matter dominated in their dynamics. In contrast for the gas rich UDGs, the gaseous component contributes significantly...
Figure 2. A Gaussian smoothed (σ = 0.5 Å) KCWI spectrum for Y358 (black) with example pPXF fit (red). Residuals from the non-smoothed fit are show at the bottom (blue). The spectrum, fit and residuals are displayed at the observed wavelengths. The prominent Hβ and Mg b triplet absorption features are indicated by dashed vertical lines.

Table 1. Pertinent properties of UDG samples relating to the discussion of Figure 4. From left to right columns are: 1) Sample description. When relevant the simulation name is given before the literature reference; 2) Stellar mass range; 3) Halo mass range; 4) Environment; and 5) Gas content of the sample. The halo mass range of Cardona-Barrero et al. (2020) was not published in that work and was provided upon request by the corresponding author.

| Sample                  | Log($M_\star/M_\odot$) | Log($M_{\text{halo}}/M_\odot$) | Environment | Gas Content |
|-------------------------|------------------------|----------------------------------|-------------|-------------|
| Observed: Y358          | 8.14                   | 11.06 – 11.22                    | Cluster     | None        |
| Observed: GC-Rich       | 8.04 – 8.89            | > 11                             | Cluster/Group | None        |
| Observed: GC-Poor       | 8.41 – 8.76            | < 11                             | Cluster     | None        |
| Observed: Kong+ (2022)  | 7.45 – 8.35            | 9.86 – 10.76                     | Field       | Rich        |
| NIHAO: Di Cintio+ (2017)| 6.83 – 8.4             | 10.22 – 10.85                    | Field       | Rich        |
| NIHAO: Jiang+ (2018)    | 6.8 – 8.8              | 9.9 – 11.1                       | Field/Group | Rich        |
| NIHAO: Cardona-Barrero+ (2020)| 6.5 – 9.0 | 10.04 – 11.29                     | Field       | Rich        |
| FIRE: Chan+ (2018)      | 7.72 – 8.44            | 10.34 – 10.74                    | Field       | None        |

It is clear from Figure 4 upper that the GC-rich UDGs have dynamical masses that are too high to agree with the best fitting dark matter halos from Kong et al. (2022). We note that this may be a reflection of the different total halo masses of the two UDG populations, i.e., the best-fitting total halo masses of the isolated, gas-rich UDG in Kong et al. (2022) are all below $10^{10.8} M_\odot$ which is less than the minimum inferred halo mass for a GC-rich UDG with $N_{GC}>20$ (10$^{11} M_\odot$; Burkert & Forbes 2020). Additionally, gas-rich UDGs to the centrally enclosed mass (see e.g., the total masses in Kong et al. 2022 table 1). We therefore choose to compare our data to the Read et al. (2016) mass profiles for the gas-rich UDGs as these trace the dark matter component of the halo which are more appropriate to compare to the measurements we are getting for our GC-rich/poor UDGs.

In Figure 4 upper we plot our dynamical mass measurement for Y358 along with dynamical mass measurements for UDGs with stellar velocity dispersions and GC counts from Gannon et al. (2022). The UDGs in this sample are generally expected to be older and gas-poor due to their association with clusters. Only one of these UDGs is not associated with a cluster (i.e., NGC 5846_UDG1) and it is in a group environment. UDGs from the Gannon et al. (2022) sample have stellar masses in the range $8.04 < \log(M_\star / M_\odot) < 8.89$. Four of the 7 Kong et al. (2022) UDGs have stellar masses in this range, with the remaining 3 having stellar masses slightly smaller (i.e., $7.45 < \log(M_\star / M_\odot) < 8.35$). Plotted mass measurements are colour coded by GC richness based on a rich/poor divide of $N_{GC} \geq 20 / N_{GC} < 20$. The halo mass implied for a GC-rich UDG with $N_{GC} \geq 20$ is $\geq 10^{11} M_\odot$ (Burkert & Forbes 2020). We summarise the pertinent properties (i.e., stellar mass, halo mass, environment and gas content) of these two observational samples in Table 1.
tend to be younger, bluer with more irregular morphologies than other UDGs (Leisman et al. 2017), likely indicating ongoing star formation. Furthermore, recent work has shown that isolated, gas-rich UDGs do not have rich GC systems (Jones et al. 2022). We conclude that gas-rich UDGs similar to those observed by Kong et al. (2022) could not evolve into the GC-rich UDGs observed at present times. The progenitors of GC-rich UDGs require more massive dark matter halos at fixed stellar mass.

This conclusion is not true for the GC-poor UDGs plotted in Figure 4. All three of these UDGs have dynamical masses in agreement with the mass profiles of Kong et al. (2022). We suggest it is possible that GC-poor UDGs in clusters have similar dark matter halo characteristics to isolated, gas-rich UDGs. Further, this suggests the processing and passive evolution of isolated, gas-rich UDGs is a possible for-
formation pathway for GC-poor UDGs in clusters. This conclusion is similar to proposals from previous works (see e.g., Román & Trujillo 2017b; Martin et al. 2019; Grishin et al. 2021). Our results therefore support GC-rich UDGs forming in more massive dark matter halos than GC-poor UDGs, with GC-poor UDGs being the possible evolution of isolated, gas-rich UDGs.

In Figure 4 lower we plot the mass range of UDG profiles modelled in the NIHAO simulations of Di Cintio et al. (2017, purple band) and in the FIRE simulations of Chan et al. (2018, orange band) vs. the observed isolated, gas-rich UDGs from Kong et al. (2022, green lines). Both simulations primarily model UDGs as ‘puffy dwarfs’ with large sizes driven by strong supernovae feedback. Both of the simulations are restricted to modelling UDGs in a relatively isolated environment, similar to the environment of Kong et al. (2022)’s observations. Additionally, the stellar mass range and total halo mass range of the UDGs modelled in the simulations provides good coverage of the stellar mass range and best-fitting total halo mass range of Kong et al. (2022)’s observed UDGs. We note, however, the recent observational work of Kado-Fong et al. (2022) which found that isolated, gas-rich UDGs do not exhibit the bursty star formation histories expected from these simulations. We summarise the stellar mass, total halo mass, environment and gas-richness of each sample in Table 1. With similar environments, stellar masses and total halo masses, we might expect these simulations to reproduce the mass profiles of the observed isolated, gas-rich UDGs.

To make this comparison, in Figure 4 lower we now plot the observed HI mass profiles from Kong et al. (2022), which include both the gaseous and stellar component of the mass along with the dark matter. The Di Cintio et al. (2017) NIHAO result plotted is also a total mass profile, including stars, gas and dark matter. Note that the FIRE mass profiles do not include gas, as they artificially quench their UDGs as part of their simulation. Without this artificial quenching their UDGs may still be expected to be gas-rich at present times. For both the Di Cintio et al. (2017) and Kong et al. (2022) data plotted in Figure 4 lower, the gas mass is, on average, more massive than the stellar component.

It is clear from Figure 4 lower that both simulations create mass profiles more massive than the isolated, gas-rich UDGs that their simulations are best matched to reproduce. This is despite having a similar total halo mass. The mass profiles from the simulations are instead more closely matched to the GC-rich UDGs plotted in the upper panel. However, few GC-rich UDGs have been observed in the low density environments such as those simulated, with some authors suggesting environment plays a key role in their GC formation (Prole et al. 2019a; Somalwar et al. 2020). Furthermore, based on their GC-richness and the GC number – halo mass relationship of Burkert & Forbes (2020), the GC-rich UDGs plotted are all expected to reside in halos of total mass greater than either the FIRE or NIHAO simulations at the same stellar mass. In order to have the observed GC-rich UDGs residing in halos with the total mass that is modelled in the simulations at the same stellar mass, they cannot follow the Burkert & Forbes (2020) relationship. We explore UDGs in stellar mass – halo mass space further in Section 3.3.

It is worth noting that further studies of UDGs in the NIHAO simulations have shown that NIHAO can model UDGs in group environments and at higher stellar masses (Jiang et al. 2019; Cardona-Barrero et al. 2020). It is therefore likely that the full mass profile range that is reproducible by the NIHAO simulations is not fully captured by what we are plotting from Di Cintio et al. (2017). However, UDGs at higher stellar masses are expected to have higher mass profiles (see Table 1). These higher stellar mass UDGs will therefore not affect the conclusions we draw from Figure 4 lower. Additionally, some of the UDG sample used in Di Cintio et al. (2017) includes galaxies that do not strictly meet the original van Dokkum et al. (2015) UDG definition (i.e., they include galaxies with $R_e < 1.5$ kpc).

### 3.3 UDGs on the Stellar Mass – Halo Mass Relationship

In Figure 5 we further investigate observed UDGs vs. the FIRE and NIHAO simulations by comparing them with the stellar mass – halo mass relationships. Y358 and GC-rich UDGs from Gannon et al. (2022) are plotted using halo mass measurements calculated from their GC-numbers (Burkert & Forbes 2020). Here we do not plot the UDGs PUDG_S74 and PUDG_R84, along with the GC-poor sample, as their exact GC counts with errors are unpublished, leading to an uncertain total halo mass. Kong et al. (2022) UDGs are plotted using the total halo mass coming from best fitting Read et al. (2016) halo profiles (see their table 1). The data for the NIHAO sample presented in Cardona-Barrero et al. (2020) were attained from the corresponding author. The data for the FIRE UDGs are taken from their table 2 (Chan et al. 2018). Stellar mass – halo mass relationships are plotted from the studies of Behroozi et al. (2013) and Moster et al. (2013).

To quantify the deviation of each sample plotted in Figure 5 from established stellar mass – halo mass relationships we define the quantity $\Delta_{SMHM}$ for a sample of size $n$. This is the average logarithmic difference between the measured halo masses $M_{\text{halo},\text{UDG}}$ and the expected halo mass at the stellar mass of each UDG $M_{\text{halo},SMHM}$ based on a stellar mass – halo mass relationship.

$$\Delta_{SMHM} = \frac{1}{n} \sum_{i=1}^{n} \log_{10} \frac{M_{\text{halo},\text{UDG}}}{M_{\text{halo},SMHM}}$$

When using Equation 2 for Behroozi et al. (2013) and Moster et al. (2013) we refer to it as $\Delta_{B13}$ and $\Delta_{M13}$ respectively. Positive values for $\Delta_{SMHM}$ indicate that the sample resides in dark matter halos that are on average more massive than the stellar mass – halo mass relationship. Negative values for $\Delta_{SMHM}$ indicate that the sample resides in dark matter halos that are on average less massive than the stellar mass – halo mass relationship. Values of $\Delta_{SMHM}$ near zero indicate the sample obeys the relationship. We summarise the values of $\Delta_{SMHM}$ in Table 2. Note that 7 of the Cardona-Barrero et al. (2020) UDGs are excluded from the calculation of $\Delta_{B13}$ as they have stellar masses below the relationship’s minimum value ($M_{\ast,\text{Min}} = 1.7 \times 10^7 M_\odot$).

It is clear from Figure 5 and Table 2 that both simulated UDG samples largely follow known stellar mass – halo mass relations

| Sample          | $n$ | $\Delta_{B13}$ [dex] | $\Delta_{M13}$ [dex] |
|-----------------|-----|----------------------|----------------------|
| Observed: Y358  | 1   | 0.49                 | 0.54                 |
| Observed: GC-Rich | 5   | 0.53                 | 0.63                 |
| Observed: Kong+ (2022) | 7   | -0.37                | -0.38                |
| NIHAO: Cardona-Barrero+ (2020) | 37  | 0.11                 | 0.16                 |
| FIRE: Chan+ (2018) | 6   | -0.03                | -0.01                |

### Table 2. A summary of the deviations from the stellar mass – halo mass relationships of Behroozi et al. (2013) and Moster et al. (2013) for each sample using Equation 2. From left to right columns are: 1) the sample; 2) the number of objects in the sample; 3) $\Delta_{B13}$, the average deviation calculated for Behroozi et al. (2013) and 4) $\Delta_{M13}$, the average deviation calculated for Moster et al. (2013). Note that Y358 is included in the calculation of the GC-rich statistics.
Figure 5. Stellar mass vs. halo mass. We plot Y358 (black border) along with other GC-rich UDGs from Gannon et al. (2022) as red squares. The isolated, gas-rich UDGs of Kong et al. (2022) UDGs are shown as green circles. The simulated FIRE UDGs are shown as orange crosses with NIHAO UDGs from Cardona-Barrero et al. (2020) as purple triangles. Stellar mass – halo mass relations are shown from Behroozi et al. (2013, grey line and shaded band) and from Moster et al. (2013, brown line and shaded band). Both simulations create UDGs that generally follow conventional stellar mass – halo mass relations. The observed GC-rich UDGs have halo masses more massive than either stellar mass – halo mass relationship at fixed stellar masses. The observed isolated, gas-rich UDGs from Kong et al. (2022) have halo masses less massive than either stellar mass – halo mass relationship at fixed stellar masses. Neither observed sample is reproduced by the FIRE or NIHAO simulations.

(average $|\Delta_{\text{SMHM}}| < 0.2$ dex). This is less than the typical scatter (0.2 dex) in these relations. The only exception is the low mass (both stellar and total halo) end of the Cardona-Barrero et al. (2020) data which does not follow Behroozi et al. (2013). In contrast, both observational samples deviate strongly from both stellar mass – halo mass relations. The isolated, gas-rich UDGs of Kong et al. (2022) reside in halos less massive than the stellar mass – halo mass relation predicts for their stellar mass ($\Delta_{\text{B13}} = -0.37$ dex; $\Delta_{\text{M13}} = -0.38$ dex). This conclusion has been reached previously for a similar UDG sample by Trujillo-Gomez et al. (2022). Note also that, it is unlikely that the low halo masses of these UDGs are caused by tidal stripping due to their isolated environments. The GC-rich UDG sample (which includes Y358) resides in halos more massive than the stellar mass – halo mass relationship predicts for their stellar mass ($\Delta_{\text{B13}} = 0.53$ dex; $\Delta_{\text{M13}} = 0.63$ dex). Despite both FIRE and NIHAO reproducing the observed dynamical masses of GC-rich UDGs (Fig. 4) they do not reproduce their inferred halo mass at their stellar mass.

4 EXTENDED LITERATURE SAMPLE

For the remainder of this paper, we supplement our data for Y358 with data taken from the literature for spectroscopically studied UDGs. We take those galaxies from the literature that meet a UDG definition of $R_e > 1.5$ kpc and $\langle \mu_V \rangle_e > 24.7$ mag arcsec$^{-2}$. Our surface brightness criterion is simply that used in Gannon et al. (2022), $\langle \mu_R \rangle_e > 25$ mag arcsec$^{-2}$, transformed into $V$-band with a colour of $V = g - 0.3$. We have identified 21 galaxies in the literature meeting this definition with basic properties to place them in mass–radius–luminosity space. These properties (i.e., identifier, environment, distance, Mag., $\langle \mu_V \rangle_e$, stellar mass, $R_e$, recessional velocity, velocity dispersion and GC counts) are listed in Table A1. We include notes as to the construction of this sample in Appendix A.

4.1 UDG Spectroscopic Sample Biases

We note our UDG sample originates from a wide range of literature sources and therefore is not complete. We therefore briefly mention two obvious biases in the sample. Namely, UDGs in our literature sample tend to be 1) larger and 2) brighter in surface brightness than the broader UDG population.

In Figure 6 we plot a histogram of UDG sizes for both our literature UDG sample and a subset of the $R$-band Coma cluster catalogue of Yagi et al. (2016) that are UDGs ($R_e > 1.5$ kpc and $\langle \mu_R \rangle_e > 25$ mag arcsec$^{-2}$). We use this sample due to their likely association with the Coma Cluster which will decrease the uncertainty in their true size in comparison to a UDG sample of unknown distance. The use of a catalogue in a different filter band is expected to have only a small ($\approx 10\%$) effect on half-light radii (see e.g., the UDG fitting in table 2 of Saifollahi et al. 2022) which is not large enough to affect our results. Performing a Kolmogorov–Smirnov test, it is highly unlikely that our UDG sample was randomly selected from the UDGs in the Yagi et al. (2016) catalogue ($p$ value $= 0.005$). Our literature sample is larger, with median half-light radius (2.8 kpc) larger than the Yagi et al. (2016) catalogue (median half-light radius 1.83 kpc).

In Figure 7 we plot a histogram of the surface brightnesses of our literature UDG sample. We include for comparison UDG candidates from the Stripe 82 SMUDGes catalogue of Zaritsky et al. (2021).
Figure 6. Normalised histograms of UDG circularised half-light radii. We plot our UDG sample ($N = 21$; orange solid line) in comparison to the Yagi et al. (2016) $R$-band catalogue of Coma cluster objects that are UDGs ($N = 153$; blue dashed line). Median values for each sample are indicated by arrows at the top of the plot. Our UDG sample has generally larger half-light radii than the Coma sample.

Here we do not reuse the Yagi et al. (2016) catalogue due to the need for a common filter band to compare surface brightnesses. Additionally, the Zaritsky et al. (2021) catalogue provides the benefit of having UDGs across a full range of environments (field to cluster). For the Zaritsky et al. (2021) data we convert their measured central surface brightnesses to the average within the half-light radius using equation 11 of Graham & Driver (2005) for comparison to our other data. We also correct this $g$-band catalogue into $V$-band using $V = g - 0.3$. Performing a Kolmogorov–Smirnov test, it is unlikely that our UDG sample was randomly selected from the Zaritsky et al. (2021) catalogue ($p$ value $= 0.012$). Our literature sample has a median surface brightness (25.6 mag arcsec$^{-2}$) brighter than the Zaritsky et al. (2021) catalogue (median surface brightness 26.1 mag arcsec$^{-2}$). We note that this is despite the Zaritsky et al. (2021) catalogue containing blue UDGs which will create a bias in their sample to be brighter due to their younger ages.

To further contextualise our literature sample we show a histogram of their distances in Figure 8. We plot the peak of the GC luminosity function at each distance based on an assumed peak of $M_V = -7.3$ (Miller & Lotz 2007). We also include a number of commonly studied clusters. To date, no UDGs have been targeted for deep spectroscopy at distances beyond 100 Mpc.

In order to best establish dark matter halo profile parameters, accurate radial mass profiles are required. For UDGs, a thorough exploration of their likely cored dark matter halos will require observations to be made beyond the dark matter core radius ($\sim 5 - 10$ kpc). The current single mass measurements available for many UDGs are insufficient to truly establish dark matter halo parameters due to degeneracies in their comparison to theoretical halo mass profiles (Gannon et al. 2021). GCs pose a promising avenue to get larger radius mass estimates for UDGs to help probe their halo profile (e.g., Gannon et al. 2020). Importantly this suggests UDG observational efforts should be focused on those candidates nearby enough to allow spectroscopic studies of their GC system.

5 DISCUSSION: MASS–RADIUS–LUMINOSITY SPACE

In Figure 9 we place UDGs in mass–radius–luminosity space, an altered form of the fundamental plane for pressure-supported systems. We establish the locus traced by non-UDGs using data from Tollerud et al. (2011); Toloba et al. (2012); McConnachie (2012); Kourkchi et al. (2012) and Forbes et al. (2018). For Toloba et al. (2012) galaxies we convert half-light radii into physical units using an assumed Virgo cluster distance of 16.5 Mpc. We place Kourkchi et al. (2012) galaxies on the plane using a correction of $V = F814W + 1$. We place McConnachie (2012)$^1$ galaxies on the plane using their given Vega magnitudes. We then place our literature UDG sample on the plane to examine their location. We convert magnitudes into solar units assuming $M_{V, \odot} = 4.8$ (Willmer 2018a) and dynamical masses are calculated using Equation 1. Galaxies that fit the UDG definition in the non-UDG samples (e.g., the Sagittarius dSph appears in both McConnachie 2012 and Forbes et al. 2018) are removed before plotting as they are included in our literature sample.

We note two UDGs plotted, Andromeda XIX and Antlia II, have

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$^1$ January 2021 public version
half-light luminosities noticeably less bright than the remaining population. These galaxies have measured velocity dispersions only due to their extremely close distances (i.e., both are in the Local Group) which allows their stars to be resolved. We note that there exists a continuum of galaxies of large size and varying luminosity between these galaxies and the remaining UDGs on the relation (see e.g., table 2 of Karachentsev et al. 2017). The empty region between these galaxies and the remainder of our sample is simply a side effect of our bias to higher surface brightness objects. For the remainder of our discussion we will focus on the higher-luminosity objects more readily studied.

Interestingly, UDGs reside in a region of parameter space largely separate from the locus of non-UDGs. Their main difference is simply their larger half-light radii, with dynamical masses and luminosities similar to the lens of non-UDGs (the empty region between these two populations in half-light radii on Figure 9 exists due to selection effects). An unfortunate corollary of UDGs inhabiting an entirely new parameter space is that, at fixed luminosity, UDG masses cannot be estimated from luminosity and radius information alone. This will hamper efforts to perform statistical estimations of UDG masses based on their photometric properties (e.g., Zaritsky 2017; Lee et al. 2020).

The similarity in luminosities between UDGs and non-UDGs have led many to suggest they may simply be an extension of the dwarf galaxy population to larger sizes (see e.g., Conselice 2018). These UDGs could be ‘puffy’ dwarf galaxies formed through conventional pathways (e.g., Amorisco & Loeb 2016; Di Cintio et al. 2017; Rong et al. 2017; Tremmel et al. 2020). A likely example of these are the GC-poor, cluster UDGs plotted in Figure 4 which are plausibly the result of the transformation of extended, star forming field dwarfs (e.g., Grishin et al. 2021). In mass–radius–luminosity space ‘puffy dwarf’ UDGs are expected to have similar luminosities, larger radii and dynamical masses only slightly larger than their non-UDGs of similar luminosity. This is reflective of their similar dark matter halos. Much of our literature sample has mass, radius and luminosity compatible with this expectation for a ‘puffy dwarf’ formation scenario.

We caution that this expectation for ‘puffy dwarf’ UDGs may be over-simplified. Kadowaki et al. (2021) found that the dynamical masses of UDGs measured with increasingly large radii likely correspond to increasingly massive dark matter halos (see their appendix A). In this framework, many of the UDGs in our sample may have dynamical masses corresponding to dark matter halos more massive than non-UDGs at similar luminosity. If this is the case, these UDGs cannot be explained by ‘puffy dwarf’ formation scenarios due to their massive dark matter halos. We do note however, that due to the bias to UDGs with larger half-light radius in our sample, we expect a greater fraction of our sample to be massive halo UDGs than the UDG population as a whole.

Finally, we suggest Figure 9 is a fundamental empirical plot that should be reproduced by galaxy formation simulations focusing on UDGs. Particularly, many simulations currently have difficulty reproducing the full range of dwarf galaxy sizes. For example the ROMULUS-C simulations currently form the majority of their dwarfs in the UDG stellar mass regime as UDGs (see Tremmel et al. 2020 table 1). In addition, UDG studies using the Illustris simulations have to assign their UDG candidates sizes due to limitations of their simulations (Carleton et al. 2019; Sales et al. 2020). Simulations reproducing the full range of galaxy sizes and masses in the UDG luminosity regime will be crucial to developing a theoretical understanding of their formation.

6 CONCLUSIONS

In this work we have added Keck/KCWI spectroscopy of a GC-rich, Coma cluster UDG, Y358, to the literature. We then create a literature sample of UDGs that have been studied spectroscopically, placing them in mass–radius–luminosity space for pressure-supported galaxies. Our main conclusions are as follows:

- We measure a recessional velocity (7969 ± 2 km s⁻¹) and velocity dispersion (19 ± 3 km s⁻¹) for Y358. The recessional velocity confirms its association with the Coma cluster. This association formalises the distance of Y358 and its status as a UDG.
- We measure an average velocity of 22 km s⁻¹ for Y358 and compare it to cuspy and cored dark matter halo profiles with total mass inferred from its GC count. Under the assumption that the total halo mass from GC counts is correct, Y358 likely resides in a cored dark matter halo.

We supplement our dynamical mass measurement for Y358 with others from Gannon et al. (2022). We then compare to the best-fitting dark matter mass profiles for isolated, gas-rich UDGs from Kong et al. (2022). We also compare the Kong et al. (2022) measurements to simulations of UDG formation from the NIHAO suite (Di Cintio et al. 2017) and the FIRE suite (Chan et al. 2018). We find:

- The GC-poor UDGs may reside in a dark matter halo of similar radial profile to the isolated, gas-rich UDGs of Kong et al. (2022), suggesting an evolutionary connection may exist between the two populations. Dynamical mass measurements made for GC-rich UDGs are sufficiently high to exclude them residing in dark matter halos similar to the isolated, gas-rich UDGs. We suggest it is unlikely that GC-rich UDGs represent an evolved population of isolated, gas-rich UDGs.

Figure 8. A histogram of UDG distances for UDGs from our literature sample. The x-axis shows the Distance (Mpc), redshift (z) and the apparent magnitude of the GC luminosity function peak. The positions of select clusters are given along the top of the plot (vertical coloured lines). To date, no UDGs have been targeted for deep spectroscopy at distances beyond 100 Mpc.
Both the simulations of Di Cintio et al. (2017) and Chan et al. (2018) produce mass profiles for UDGs that are too massive when compared to the isolated, gas-rich UDGs of Kong et al. (2022). This is unexpected as the Kong et al. (2022) samples have the properties (i.e., stellar mass, total halo mass, environment and gas-richness) most resembling the UDG in their simulations. The simulated mass profiles are instead more consistent with GC-rich UDGs.

We find that although FIRE and NIHAO simulations cover the stellar and halo mass range of GC-rich UDGs, they cannot reproduce their observationally-estimated halo masses at the same stellar mass. This is perhaps not unexpected given that the simulations are for isolated UDGs, whereas our observed UDGs are located in groups and clusters where additional environmental effects may play a role in their evolution.

We then gather a literature sample for all galaxies meeting our UDG definition with spectroscopic velocity dispersions. We find two biases in this sample:

• The UDGs in our literature sample are on average larger than the population as a whole.
• The UDGs in our literature sample have brighter surface brightness than the population as a whole.

Both of these need to be kept in mind when considering UDG formation scenarios from current observational data. We then place our UDG sample in mass–radius–luminosity space, examining their location. We find:

• UDGs are located at a similar locus to non-UDGs of similar luminosity with the primary difference being their increased half-light radius. This supports notions that some UDGs are simply ‘puffy dwarfs’ with extended sizes driven by known physical processes.
• UDGs’ dynamical masses within their large radii may indicate massive dark matter halos not expected in a ‘puffy dwarf’ formation scenario. As our UDG sample is biased to the largest systems, we suggest a greater fraction of UDGs in our sample may be massive halo UDGs than the population as a whole.
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DATA AVAILABILITY

The KCWI data presented are available via the Keck Observatory Archive (KOA): https://www2.keck.hawaii.edu/koa/public/koa.php 18 months after observations are taken. The literature sample discussed is included in Appendix A.

Y358 and Literature UDG Dynamical Masses
APPENDIX A: LITERATURE UDG DATA

In this Appendix we present the literature sample of spectroscopically analysed UDGs used in Section 4. Lettering in the notes below corresponds to the superscripts in Table A1.

A0.1 Y358

Notes: \( a = \) Calculated from the absolute magnitude assuming \( M_\star/L_V = 2 \) and \( M_{\odot}/V = 4.8 \) (Willmer 2018b). \( b = \) Circularised using literature \( b/a \) (0.83; van Dokkum et al. 2017). Data sources: This work, van Dokkum et al. (2017) and Lim et al. (2018).

A0.2 VCC 1287

Notes: \( a = \) This galaxy is identified as NGVSUDG-14 in Lim et al. (2020). \( b = \) It is unclear which filter band this is in, although g-band seems likely from the context. We therefore transform it into V-band using \( V = g - 0.3 \). Data sources: Beasley et al. (2016); Gannon et al. (2020, 2021); Lim et al. (2020).

A0.3 DGSAT I

Notes: \( a = \) It is located in the Pisces–Perseus supercluster and could potentially be a ‘backsplash’ galaxy (Martínez-Delgado et al. 2016; Papastergis et al. 2017). \( b = \) Calculated using the properties listed in Table 2 of Martínez-Delgado et al. (2016) and equation 11 of Graham & Driver (2005). \( c = \) Circularised using literature \( b/a \). \( d = \) Note that some of these GC’s may be overluminous (Janssens et al. 2022). Data sources: Martínez-Delgado et al. (2016); Martín-Navarro et al. (2019); Janssens et al. (2022).

A0.4 Dragonfly 44

Notes: \( a = \) Although in the direction of the Coma cluster “it is unclear whether Dragonfly 44 is in a cold clump that is falling into the cluster, a filament, or a structure that is unrelated to Coma” (van Dokkum et al. 2019). \( b = \) Calculated using the properties listed in Table 1 of van Dokkum et al. (2017) at a distance of 100 Mpc and equation 11 of Graham & Driver (2005). \( c = \) Converted using \( V_R = c \times \ln(1 + z) \) from the redshift listed in footnote 6 of van Dokkum et al. (2017). \( d = \) Note the \( N_{GC} \) quoted in the abstract is slightly different to this value. Here we use the value from Table 1 of van Dokkum et al. (2017). \( e = \) Although see Saifollahi et al. (2021) for a differing view of the GC.
richness of Dragonfly 44. Data sources: van Dokkum et al. (2016, 2017, 2019); Gannon et al. (2021).

A0.5 DF2X1

Notes: $a = \text{Calculated using the properties listed in Table 1 of van Dokkum et al. (2017) at a distance of 100 Mpc and equation 11 of Graham & Driver (2005)}$. $b = \text{Converted using } V_R = c \ln(1 + z)$ from the redshift listed in section 2.1 of van Dokkum et al. (2017). $c = \text{it is unclear if this is also effected by the barycentric correction issue described in footnote 16 of van Dokkum et al. (2019)}$. Data sources: van Dokkum et al. (2017); Gannon et al. (2021).

A0.6 NGC 5846_UDG1

Notes: $a = \text{This galaxy is referred to as MATLAS-2019 in the MATLAS dwarf galaxy catalog (Habas et al. 2020; Müller et al. 2020, 2021)}$. $b = \text{Calculated using the properties listed in Table 1 of Forbes et al. (2019) and equation 11 of Graham & Driver (2005). Transformed from g-band using } V = g - 0.3$. $c = \text{We prefer these values over those reported in Müller et al. (2020) due to the greater instrumental resolution of Keck/KCWI over VLT/MUSE. } d = \text{We prefer these values over those reported in Müller et al. (2021) due to the deeper HST data used. Data sources: Müller et al. (2020, 2021); Forbes et al. (2021); Danieli et al. (2022).}$

A0.7 VLSB-B

Notes: $a = \text{This galaxy is identified as NGVSDUDG-11 in Lim et al. (2020)}$. $b = \text{Vega magnitude. } c = \text{Circularised using literature ellipticity. } d = \text{This is a GC system velocity dispersion that we assume is equivalent to the stellar velocity dispersion of the galaxy based on the evidence for this assumption in Forbes et al. (2021). Data sources: Toloba et al. (2018); Lim et al. (2020).}$

A0.8 VLSB-D

Notes: $a = \text{VLSB-D has an elongated structure and velocity gradient (Toloba et al. 2018) that suggests it is undergoing tidal stripping. } b = \text{This galaxy is identified as NGVSDUDG-04 in Lim et al. (2020)}$. $b = \text{Vega magnitude. } c = \text{Circularised using literature ellipticity. } d = \text{This is a GC system velocity dispersion that we assume is equivalent to the stellar velocity dispersion of the galaxy based on the evidence for this assumption in Forbes et al. (2021). Data sources: Toloba et al. (2018); Lim et al. (2020).}$

A0.9 VCC 615

Notes: $a = \text{This galaxy is identified as NGVSDUDG-A04 in Lim et al. (2020)}$. $b = \text{Vega magnitude. } c = \text{Circularised using literature ellipticity. } d = \text{This is a GC system velocity dispersion that we assume is equivalent to the stellar velocity dispersion of the galaxy based on the evidence for this assumption in Forbes et al. (2021). Data sources: Toloba et al. (2018); Lim et al. (2020); Mihos et al. (2022).}$

A0.10 UDG1137+16

Notes: $a = \text{UDG1137+16 has a disturbed morphology making it likely it is undergoing stripping (Gannon et al. 2021). } a = \text{See also Müller et al. (2018) who refer to this galaxy as ‘dw1137+16’. Transformed to V-band using stated } g-r \text{ colour and } V = g - 0.3$. $c = \text{Calculated using the properties listed for the single Sérsic fit in Table 1 of Gannon et al. (2021) and equation 11 of Graham & Driver (2005). Data source: Gannon et al. (2021).}$

A0.11 PUDG-R15

Notes: $a = \text{Transformed from g-band using } V = g - 0.3$. $b = \text{Circularised using literature } b/a$. Data source: Gannon et al. (2022).

A0.12 PUDG-R16

Notes: $a = \text{Transformed from g-band using } V = g - 0.3$. $b = \text{Circularised using literature } b/a$. Data source: Gannon et al. (2022).

A0.13 PUDG-S74

Notes: $a = \text{Transformed from g-band using } V = g - 0.3$. $b = \text{Circularised using literature } b/a$. Data source: Gannon et al. (2022).

A0.14 PUDG-R84

Notes: $a = \text{Transformed from g-band using } V = g - 0.3$. $b = \text{Circularised using literature } b/a$. Data source: Gannon et al. (2022).

A0.15 NGC 1052-DF2

Notes: $a = \text{This galaxy has both an anomalous star cluster system (van Dokkum et al. 2018b; Shen et al. 2021) and an abnormally low velocity dispersion (van Dokkum et al. 2018a; Danieli et al. 2019). There is also evidence it may be undergoing a tidal interaction (Keim et al. 2022, although see Montes et al. 2021). We do however note there is some evidence for rotation in NGC 1052-DF2 which may help alleviate the paucity of dark matter implied by its low velocity dispersion (Lewis et al. 2020; Montes et al. 2021). } a = \text{This is also catalogued as [KKS2000]04 in Karachentsev et al. (2000). } b = \text{While there existed some initial controversy over the distance of NGC 1052-DF2 (see e.g., Trujillo et al. 2019; Monelli & Trujillo 2019) we believe the deeper data reported in Shen et al. (2021) resolved this issue. We note however, despite an established distance this does not fully establish an environmental association for NGC 1052-DF2 (see e.g., Fig. 5 of Shen et al. 2021). The possibility exists that NGC 1052-DF2 was part of the NGC 1052 group but now resides outside of the group as a consequence of its formation (e.g., van Dokkum et al. 2022). } c = \text{Calculated using the properties listed for the single Sérsic fit in Table 2 of Cohen et al. (2018) and equation 11 of Graham & Driver (2005). } d = \text{We prefer these values over those reported in Emsellem et al. (2019) due to the greater instrumental resolution of Keck/KCWI over VLT/MUSE. } e = \text{Here we use the value of GCs in the roughly expected GC luminosity function window as reported by Shen et al. (2021). This value excludes the brighter sub-population. Data sources: Danieli et al. (2019); Shen et al. (2021).}$

A0.16 Sagittarius dSph

Notes: $a = \text{Note this galaxy is known to be tidally disrupting around the Milky Way (Ibata et al. 2001). } a = \text{Calculated using the properties listed in Table 1 of Forbes et al. (2018) and equation 12 of Graham & Driver (2005). Data sources: McConnachie (2012); Karachentsev et al. (2017); Forbes et al. (2018).}$
**A0.17 Andromeda XIX**

*Notes:* Note this galaxy is likely affected by tidal processes interacting with the nearby M31 (Collins et al. 2020). \(a\) = Calculated using the properties listed in Table 3 of Collins et al. (2020) and equation 12 of Graham & Driver (2005). Due to the extremely diffuse nature of this object this value is highly uncertain. Data sources: Martin et al. (2016); Collins et al. (2020); Gannon et al. (2021).

**A0.18 Antlia II**

*Notes:* Dynamical modelling suggests that a combination of a cored dark matter profile and tidal stripping may explain the properties of this UDG (Torrealba et al. 2019). \(a\) = Vega magnitude. \(b\) Due to the extremely faint nature of Antlia II this value is highly uncertain. Data sources: McConnachie (2012); Torrealba et al. (2019)

**A0.19 WLM**

*Notes:* WLM is gas-rich and undergoing active star formation (Leaman et al. 2009). \(a\) = calculated from given \(m - M\). \(b\) = Vega magnitude. \(c\) Calculated using equation 12 of Graham & Driver (2005). \(d\) = Calculated from \(V\)-band magnitude assuming \(M_\star/L_V\) = 2. Data sources: McConnachie (2012); Forbes et al. (2018)

**A0.20 J125929.89+274303.0**

*Notes:* \(a\) = Converted from \(R\)-band using \(V = R + 0.5\) (based on Virgo dE’s; van Zee et al. 2004) Data sources: Chilingarian et al. (2019); Gannon et al. (2021).

**A0.21 J130026.26+272735.2**

*Notes:* \(a\) = Converted from \(R\)-band using \(V = R + 0.5\) (based on Virgo dE’s; van Zee et al. 2004) Data sources: Chilingarian et al. (2019); Gannon et al. (2021).
| Name                  | Env.          | $D$ [Mpc] | $M_V$ [mag] | $\langle \mu_V \rangle_e$ [mag arcsec$^{-2}$] | $M_*$ [$\times 10^8$ $M_\odot$] | $R_e$ [kpc] | $V_R$ [km s$^{-1}$] | $\sigma$ [km s$^{-1}$] | $N_{GC}$ |
|----------------------|---------------|-----------|-------------|---------------------------------------------|---------------------------------|-------------|---------------------|----------------------|----------|
| Y358                 | Cluster {Coma} | 100       | -14.8       | 25.6                                        | 1.38$^a$                        | 2.1$^b$     | 7969 (2)           | 19 (3)               | 28 (5.3) |
| VCC 1287$^a$         | Cluster {Virgo}| 16.5      | -15.6       | 25.71$^b$                                   | 2                               | 3.3         | 1116 (2)           | 19 (6)               | 22 (8)   |
| DGSAT 1              | Field$^a$     | 78        | -16.3       | 25.6$^b$                                     | 4                               | 4.4$^c$     | 5439 (8)           | 56 (10)              | 12 (2)$^d$ |
| Dragonfly 44         | Cluster$^b$ {Coma} | 100     | -16.2       | 25.7$^b$                                     | 3                               | 3.9         | 6324$^c$           | 33 (3)               | 76 (18)$^{d,e}$ |
| DFX1                 | Cluster {Coma} | 100       | -15.8       | 25.5$^a$                                     | 3.4                             | 2.8         | 8107$^b$           | 30 (7)$^c$            | 63 (17)  |
| NGC 5846_UDG1$^a$    | Group {NGC 5846} | 26.5     | -15.0       | 25.2$^b$                                     | 1.1                             | 2.1$^d$     | 2167 (2)$^c$       | 17 (2)$^c$            | 54 (9)$^d$ |
| VLSB-B$^a$           | Cluster {Virgo} | 16.5     | -13.5       | 27.5                                         | 0.06                            | 2.6$^c$     | 47 (53), -29$^d$   | 26.1 (9.9)           |          |
| VLSB-D$^a$           | Cluster {Virgo} | 16.5     | -16.2$^b$   | 27.6                                         | 0.79                            | 9.0$^c$     | 1033.8 ($^{+22.4}_{-18.8}$) | 16 (+6, -4)$^d$      | 13 (6.9) |
| VCC 615$^a$          | Cluster {Virgo} | 17.7     | -14.7$^b$   | 25.8                                         | 0.21                            | 2.3$^c$     | 2094.0 ($^{+11.0}_{-11.0}$) | 32 (+17, -10)$^d$    | 30.3 (9.6) |
| UDG1137+16$^a$       | Group {UGC 6594} | 21.1     | -14.65$^b$  | 26.5$^b,c$                                   | 1.4                             | 3.3         | 1014 (3)           | 15 (4)               |          |
| PUDG-R15             | Cluster {Perseus} | 75      | -15.65$^a$  | 24.83$^a$                                    | 2.59                            | 2.46$^b$    | 4762 (2)           | 10 (4)               |          |
| PUDG-R16             | Cluster {Perseus} | 75      | -15.9$^a$   | 25.4$^a$                                     | 5.75                            | 3.51$^b$    | 4679 (2)           | 12 (3)               |          |
| PUDG-S74             | Cluster {Perseus} | 75      | -16.49$^a$  | 24.82$^a$                                    | 7.85                            | 3.52$^b$    | 6215 (2)           | 22 (2)               |          |
| PUDG-R84             | Cluster {Perseus} | 75      | -15.4$^a$   | 24.68$^a$                                    | 2.20                            | 1.97$^b$    | 4039 (2)           | 19 (3)               |          |
| NGC1052-DF2$^a$      | Group {NGC 1052} | 22.1     | -15.3       | 24.8$^c$                                     | 2                               | 2           | 1805 (1.1)$^d$     | 8.5 (+2.3, -3.1)$^d$ | 7.1 (+7.33, -4.34)$^e$ |
| Sagittarius dSph     | Group {Local}  | 0.02      | -15.5       | 25.13$^a$                                    | 1.32                            | 2.6         | 140 (2)            | 11.4 (0.7)           | 8        |
| Andromeda XIX        | Group {Local}  | 0.93      | -10         | ~31$^a$                                      | 0.0079                          | 3.1         | -109 (1.6)         | 7.8 (+1.7, -1.5)     |          |
| Antlia II            | Group {Local}  | 0.132     | -9.03$^a$   | ~31.9$^b$                                    | 0.0088                          | 2.9         | 290.7 (1.5)        | 5.71 (1.08)          |          |
| WLM                  | Group {Local}  | 0.93$^a$  | -14.25$^b$  | 26.16$^c$                                    | 0.41$^d$                        | 2.34        | -130 (1)           | 17.5 (2)             | 1        |
| J125929.89+274303.0  | Cluster {Coma} | 100      | -14.88$^a$  | 25.17$^a$                                    | 1.12                            | 2.1         | 4928 (4)           | 21 (7)               |          |
| J130026.26+272735.2  | Cluster {Coma} | 100      | -16.27$^a$  | 24.83$^a$                                    | 1.56                            | 3.7         | 6939 (2)           | 19 (5)               |          |

Table A1. Rows from left to right are: 1) Name, 2) Environment {Name}, 3) Distance - although note this is frequently the assumed distance, 4) $V$-band absolute magnitude, 5) Average $V$-band surface brightness within the half-light radius, 6) Stellar mass, 7) 2D circularised half-light radius, 8) Recessional velocity, 9) Velocity dispersion from stars or GCs and 10) GC system number. When relevant errors are given in (brackets) after values. Values unknown are indicated with a "-". Notes on data are included with superscript letters.
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