The Harmonic and Sideband Structure of the Kilohertz Quasi-Periodic Oscillations in Sco X-1

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ABSTRACT

We use data from the Rossi X-ray Timing Explorer to search for harmonics and sidebands of the two simultaneous kilohertz quasi-periodic oscillations (kHz QPOs) in Sco X-1. We do not detect any of these harmonics or sidebands, with 95\% confidence upper limits to their power between \(\sim 1\%\) and \(\sim 10\%\) of the power of the upper kHz QPO. The oscillations produced at these frequencies may be attenuated in a scattering corona around the neutron star. We find that upper limits to the unattenuated power of some of the strongest theoretically predicted harmonics and sidebands are as low as \(\sim 2\%\) of the unattenuated power of the high-frequency QPO in Sco X-1.

Key words: accretion, accretion discs – stars: neutron – stars: Sco X-1 – X-rays: stars

1 INTRODUCTION

It is four years now since the kilohertz quasi-periodic oscillations (kHz QPOs) were discovered in the persistent flux of Scorpius X-1 (van der Klis et al. 1996a) and 4U 1728-34 (Strohmayer, Zhang & Swank 1996). In the meantime, similar kHz QPOs have been seen in 20 other low-mass X-ray binaries (LMXBs; see van der Klis 2000 for a review). These QPOs often appear in pairs, with frequencies \(\nu_1\) and \(\nu_2\) \((\nu_2 > \nu_1)\) between \(\sim 400\) and \(\sim 1300\) Hz, which in a given source can shift by a few hundred Hz, apparently as a function of mass accretion rate.

Most of the models proposed so far assume that one of the kHz QPOs reflects the Keplerian orbital motion at some preferred radius in the accretion disc (e.g., Miller, Lamb & Psaltis 1998; Stella & Vietri 1999; Osherovich & Titarchuk 1999), but there are other explanations as well (Klein et al. 1996a,b; Jernigan, Klein & Arons 2000). In recent discussions (Lamb & Miller 1999; Stella 1999; Psaltis 1999) it was emphasized that empirical discrimination between two of the leading classes of models is possible in principle by studying the harmonic and sideband structure of the kHz QPOs. Here we concentrate only on these two model classes.

In the ‘sonic-point’ model (SPM; Miller et al. 1998), the QPO at \(\nu_2\) (the upper QPO) is produced at the radius where the radial flow velocity in the disc turns from subsonic to supersonic (the sonic radius), and the QPO at \(\nu_1\) (the lower QPO) originates by a beat between the upper QPO and the spin frequency of the neutron star. In the ‘relativistic-precession’ model (RPM; Stella & Vietri 1999) the QPO at \(\nu_2\) is also assumed to be Keplerian, but the QPO at \(\nu_1\) is produced by the apsidal precession of a slightly non-circular inner accretion disc. The QPO frequencies in the RPM are calculated for test particles in purely geodesic relativistic motion, i.e., neglecting the hydrodynamical and radiative effects of the accretion flow. However, Psaltis & Norman (2000) have recently proposed a dynamical model in which the QPOs are produced by oscillations in the accretion disk. In this model, which we will call ‘transition-radius’ model (TRM), there is a transition radius in the accretion disc that acts as a band-pass filter with resonances near the orbital and periastron-precession frequencies.

Besides the main peaks at \(\nu_1\) and \(\nu_2\), the SPM and the TRM predict other (weaker) harmonics and sidebands of these QPOs, at specific frequencies. For instance, the SPM predicts a relatively strong harmonic of the lower QPO at \(2\nu_1\) (see Table 3 of Miller et al. 1998 for a list of other sideband peaks predicted by the SPM), whereas the TRM predicts a sideband at \(2\nu_2 - \nu_1\) (cf. eq. [29] in Psaltis & Norman 2000). In principle, the detection of a QPO at \(2\nu_1\) and a non-detection of a QPO at \(2\nu_2 - \nu_1\) would tend to rule out the TRM, whereas the detection of a QPO at \(2\nu_2 - \nu_1\) and a non-detection of a QPO at \(2\nu_2 - \nu_1\) would tend to rule out the SPM (Miller 2000).

In this Letter, we use data from the Rossi X-ray Timing Explorer (RXTE) to search for the predicted harmonics and sidebands in the power spectrum of the kHz QPO source Sco X-1. Because of its very high flux, Sco X-1 has extremely significant kHz QPOs, and hence a very sensitive study of
any harmonic structure is possible. We do not detect any of these secondary QPOs. The fact that we detect the kHz QPOs at \( \nu_1 \) and \( \nu_2 \), but none of these other peaks sets severe constraints on the models currently proposed to explain the kHz QPOs in LMXBs.

2 OBSERVATIONS

We used data from the Proportional Counter Array (PCA; Jahoda et al. 1996) on board RXTE (Bradt, Rothschild & Swank 1993) taken on 1996 February 14, 18, 19, 1996 May 24 – 28, 1997 March 15, 1997 April 18 – 24, 1997 August 22, 1998 January 2 – 8, 1998 February 27, 28, 1998 May 30, 31, 1998 June 1, 2, 1998 July 2 – 5, 1999 January 6, 8 – 11 and 13 – 16. Each observation (i.e., each part of the data with a unique RXTE ID number) consists of data blocks of \( \sim 60 \) s interrupted by passages of the satellite through the South Atlantic Anomaly and occultations of the source by the Earth. The total usable time was \( \sim 630 \) ks.

To avoid detector safety triggers, telemetry saturation, and to reduce the dead-time effects produced by the high count rate of Sco X-1, some observations were carried out with the source slightly off-axis, with some of the five proportional counter units of the PCA switched off, recording only photons detected by the upper anode chain of the PCA, recording only photons from a limited energy range, or using a combination of these constraints. In all cases, high-time resolution data were available with a time resolution of 0.25 ms or better. For our analysis below we combined all the available data, irrespective of whether they were collected using any of the above observational constraints. When single and double-event data were recorded in parallel (see van der Klis et al. 1996b), we combined them off-line to enhance the sensitivity.

3 ANALYSIS AND RESULTS

We divided the high time resolution data into 16 s segments, and produced a power spectrum for each of these segments up to a Nyquist frequency of 2048 Hz (for \( \sim 50 \% \) of the data we also produced power spectra up to a Nyquist frequency of 4096 Hz). For 69\% of the observations the power spectra were calculated using the full PCA energy band. For the rest of the power spectra we used data from selected energy bands (24\% of the power spectra were calculated between 5 – 18 keV, 5\% between 5 – 60 keV, and 2\% between 2 – 18 keV) because we found that the kHz QPOs were more significant in those energy bands, or because those were the only energy bands available. Finally, we averaged together groups of 8 contiguous 16 s power spectra to produce average power spectra.

We searched these average power spectra for kHz QPOs, at frequencies \( \geq 250 \) Hz. We did this by first identifying those power spectra that showed a strong QPO, and visually estimating its frequency, \( \nu_0 \). When two QPOs were present in the power spectra, we always picked the one at higher frequency. It turned out that in the cases where only one kHz QPO was visible, it was always the upper kHz QPO (see below). We then fitted the power spectra, in the range \( \nu_0 - 100 \) Hz to \( \nu_0 + 100 \) Hz, using a function consisting of a constant, a power law and one Lorentzian. We discarded the power spectra for which the QPOs were less than 3\( \sigma \) significant. We note that in this manner we might have discarded data with weak QPOs that could have been detected averaging together more data. There were 1,384 average power spectra with significant kHz QPOs, equivalent to 177,152 s of data.

For those observations where we detected only one QPO in the average power spectra we applied the ‘shift-and-add’ technique (Méndez et al. 1998) to try and detect the second QPO: Based on the frequency of the detected QPO, we aligned and averaged all the power spectra of a single observation. In those cases, this procedure revealed a second kHz QPO, which in all cases was at a lower frequency than the QPO peak that we used to align the power spectra, showing that all the initial frequency measurements in the 1,384 average power spectra corresponded to the upper kHz QPO.

We measured the frequency separation between the kHz QPOs as a function of the upper kHz QPO frequency, \( \nu_2 \). We proceeded as follows: We aligned the 1,384 power spectra using the upper kHz QPO as a reference; we grouped the data in 49 sets, each of them containing \( \sim 40 \) to \( \sim 210 \) power spectra, such that \( \nu_2 \) did not vary by more than 5 – 10 Hz within each set, and we combined these aligned spectra to produce an average power spectrum for each set. We fitted these 49 power spectra in the range 400 – 1300 Hz using a function consisting of a constant, a power law and two Lorentzians. The fits were good, with reduced \( \chi^2 \leq 1.1 \) for 279 degrees of freedom, and the significance of both peaks was always \( > 3 \sigma \).

Fig. 1 shows that \( \Delta \nu = \nu_2 - \nu_1 \), the frequency difference between the two QPOs, decreases from \( \sim 310 \) Hz to \( \sim 240 \) Hz, as \( \nu_2 \) increases from \( \sim 840 \) Hz to \( \sim 1100 \) Hz. This figure can be compared to fig. 3a of van der Klis et al. (1997), who first reported the decrease in \( \Delta \nu \) with \( \nu_2 \) in Sco X-1. Because we included more data, and because we used the shift-and-add technique to measure \( \Delta \nu \), the errors are smaller in the present figure than in the previous one, and some structure, particularly between 900 and 1020 Hz, becomes apparent (perhaps this structure is related to the ‘bump’ seen in the
kHz QPOs in Sco X-1

Table 1. Upper limits to the observed amplitudes of the harmonics and sidebands of the kHz QPOs in Sco X-1

| Frequency range | Upper limit \(^a\) |
|-----------------|-------------------|
| \(2\nu_1\)      | 0.12              |
| \(2\nu_2\)      | 0.13              |
| \(\nu_2 - \nu_1\) | 0.30              |
| \(\nu_2 + \nu_1\) | 0.08              |
| \(2\nu_1 - \nu_2\) | 0.26              |
| \(2\nu_2 - \nu_1\) | 0.12              |
| \(2\nu_1 + \nu_2\) | 0.10              |
| \(2\nu_2 + \nu_1\) | 0.10              |
| \(2(\nu_2 - \nu_1)\) | 0.21              |

\(^a\) 95 \% confidence upper limits to the rms fractional amplitude of the QPO at the indicated frequency, in units of the observed rms fractional amplitude of the QPO at \(\nu_2\). This QPO has an amplitude between 0.6 % and 2.5 % (van der Klis et al. 1997).

Figure 2. Shifted-and-averaged power spectra of Sco X-1. The average power spectrum shown in the left panel was computed by first aligning the individual power spectra such that a QPO peak at \(2\nu_1\) would always end up at 1320 Hz, indicated by the arrow. In the right panel a QPO peak at \(2\nu_2 - \nu_1\) would similarly end up at 1284 Hz (arrow). In both panels, the vertical lines show the frequency range used to fit the data (see text). Notice that the frequency alignment also altered the apparent shapes and frequencies of the strong QPO peaks.

The plot of \(\Delta \nu\) vs. \(\nu_1\) of 4U 1608–52 at \(\nu_1 \sim 700\) Hz; see fig. 3 in Méndez et al. (1998b).

From Fig. 3 we can read off \(\nu_1\) as a function of \(\nu_2\); because we already know \(\nu_2\) for each average power spectrum, we can calculate the expected frequencies of hypothetical signals at multiples of \(\nu_1\) and \(\nu_2\), or at frequencies that are combinations of these two frequencies, for each power spectrum. As we described in §3, some of these frequencies are important in the context of the models proposed to explain the kHz QPOs.

We calculated the following quantities: \(2\nu_1\), \(2\nu_2\), \(\nu_2 - \nu_1\), \(\nu_2 + \nu_1\), \(2\nu_1 - \nu_2\), \(2\nu_1 + \nu_2\), \(2\nu_2 + \nu_1\) and \(2(\nu_2 - \nu_1)\). We then aligned, in turn, the power spectra on each of the above frequencies, and averaged them together to try and detect a signal present at any of these frequencies. We fitted these shifted and averaged power spectra in a segment of \(\sim 400\) Hz that included the expected frequency, using a constant plus a Lorentzian with the centroid fixed in each case at the expected frequency, and with a fixed FWHM of 200 Hz, approximately equal to the sum of the FWHM of each of the QPOs (van der Klis et al. 1996b). This value is about two times larger than the largest FWHM measured in the QPOs of this and other sources, and yields conservative upper limits to the unobserved harmonics and sidebands; tighter upper limits could be obtained by fixing the FWHM to a smaller value. No detections result from choosing a smaller FWHM in the current data set. In a few cases we added a power law to the fit to take account of a sloping continuum. The shape of the power spectrum at high frequencies is dominated by dead-time effects which, in the case of Sco X-1 at a count rate that exceeds \(\sim 25,000\) \(c\) \(s^{-1}\) \(PCU^{-1}\), are large and not yet sufficiently well understood to predict the shape of the high-frequency part of the power spectrum accurately. We note that a better knowledge of this effect could yield tighter upper limits than those that we report in this paper.

We did not detect a significant QPO at any of the above frequencies. As an example, in Fig. 3 we show two power spectra that were shifted to \(2\nu_2\) and to \(2\nu_2 - \nu_1\), the frequencies of the main high-frequency peaks (besides the kHz QPOs) predicted by the models of Miller et al. (1998) and Psaltis & Norman (2000), respectively.

Upper limits are shown in Table 1. To calculate these upper limits we varied the amplitude of the Lorentzian until the \(\chi^2\) of the fit increased by 2.71 with respect to the best-fitting value (95 % confidence level for a single parameter); the upper limits we quote in Table 1 represent the change in the amplitude for this change in the \(\chi^2\). Because of the observational constraints described in §3, and because we combined power spectra computed from data in different energy bands, we cannot give upper limits in units of fractional rms amplitude (van der Klis 1995); instead, all the upper limits in Table 1 are in units of the observed fractional rms amplitude of the QPO at \(\nu_2\). Any peaks at the predicted frequencies are between 11 and 156 times weaker than the peak at \(\nu_2\), which translates into rms amplitude ratios between 0.08 and 0.30.

4 DISCUSSION

We have measured the frequencies of the two simultaneous kHz QPOs, \(\nu_1\) and \(\nu_2\), in Sco X-1 in a large data set. We have used these measurements to calculate the expected frequencies of hypothetical signals at harmonics and sidebands of these QPOs, as predicted by two classes of kHz QPO models.

We used a sensitive technique to search for these harmonics and sidebands in the power spectra of Sco X-1, but none was detected. Their power is between 10 and 100 times less than the power of the upper kHz QPO (95 % confidence).

Oscillations produced close to the surface of the neutron star can be attenuated in a scattering corona. The attenuation is generally larger for oscillations produced by a pencil beam sweeping the surroundings (beaming oscillations), than for oscillations due to actual changes of the luminosity with time (luminosity oscillations; Brainerd & Lamb 1987; Kylafis & Klimis 1987; Kylafis & Phinney 1989; Miller et al. 1988). The attenuation factor (the ratio of the amplitude \(A_{\nu}\) of the oscillations at infinity to their original amplitude \(A_0\)) as a function of frequency \(\nu\), for a scattering corona of a radius \(R\) and optical depth \(\tau\) is given by:

\[
\frac{A_{\nu,\text{lum}}}{A_{0,\text{lum}}} = 2^{3/2} x e^{-x} + e^{-x}
\]
for a luminosity oscillation, and by

$$A_{\infty, \text{beam}} / A_{0, \text{beam}} \propto e^{-x}$$

for a beaming oscillation, with $x = (3\pi \nu R \tau / c)^{1/2}$ (Kylafis & Phinney 1989).

We can use these relations to calculate the largest unattenuated amplitudes allowed by the data in Table 2. Because at each frequency the upper limit on the ratio of observed amplitudes is $A_{\infty, y}(\nu) / A_{0, \text{beam}}(\nu_2)$ (Table 2), the upper limit on the ratio of unattenuated amplitudes $A_{0, y}(\nu) / A_{0, \text{beam}}(\nu_2)$ can be obtained by minimizing

$$\alpha_y(\nu) = \frac{A_{\infty, y}(\nu)}{A_{0, \text{beam}}(\nu_2)}$$

with respect to $\tau$ and $R$, with the additional constraint that $A_{\infty, \text{beam}}(\nu_2) / A_{0, \text{beam}}(\nu_2) > 0.01$ (because the QPO at $\nu_2$ is detected at an amplitude $\geq 1$%; van der Klis et al. 1997). In eqs. 3 and 4, $y$ stands either for luminosity or beaming (see eqs. 4 and 5), and we have assumed that the QPO at $\nu_2$ is a beaming oscillation (Miller et al. 1998).

The upper limits to the unattenuated amplitudes of the sidebands and harmonics of the kHz QPOs, both for luminosity and beaming oscillations, are shown in Table 2. In units of the amplitude of the QPO at $\nu_2$, the amplitudes of these harmonics and sidebands range from 0.11 to 0.54 for a luminosity oscillation, and from 0.21 to 2.16 for a beaming oscillation (assuming beaming for the QPO at $\nu_2$). From the minimization of $\alpha_y(\nu)$ at the frequencies listed in Table 2, we get that optical depths $\tau \sim 1$–10 and radii $R \sim 1$–350 km for the putative scattering cloud in Sco X-1 would be most effective at suppressing the sidebands and harmonics. These values are comparable to those obtained by Vaughan et al. (1997, 1998), $\tau \lesssim 5$ and $R \lesssim 80$ km, for 4U 1608–52 from measurements of the time lags of the kHz QPOs (see also Kaaret et al. 1999). We want to mention that the upper limits given in Table 2 have been calculated assuming properties of the scattering corona that maximize the attenuation at each frequency independently. In reality, if the corona exists it would have fixed values of $\tau$ and $R$, so that if it is effective at suppressing the oscillations at some frequencies, it will be less effective at others.

In conclusion, there is a remarkable lack of harmonic and sideband structure in the kHz QPOs of Sco X-1. None of the frequencies predicted by the two main classes of models are detected, with upper limits implying they are one to two orders of magnitude weaker in power than the main peaks. This sets severe constraints on either the purity of the kHz QPO generation mechanism in Sco X-1, or the parameters of the scattering corona that surrounds the neutron star.

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