Application of an Improved Mayr-Type Arc Model in Pyro-Breakers Utilized in Superconducting Fusion Facilities

Jun He 1,2,* , Ke Wang 2 and Jiangang Li 2,3

Abstract: Pyro-breaker, a fast-responding, highly reliable and explosive-driven circuit breaker, is utilized in several Quench Protection Systems (QPS). The commutation process and its parameters are the main technical considerations in the process of designing a new pyro-breaker. The commutation parameters, such as the commutation time and the current change rate, are not only determined by the electrical parameters of the commutation circuit but also the arc behavior during the operation. The arc behavior is greatly affected by the structure and the driving mechanism of the Commutation Section (CS) in the pyro-breaker. The arc model was developed decades ago and the black-box arc model is considered a valid method to study arc behavior. In this paper, the Schavemaker black-box arc model, an improved Mayr-type arc model, is applied to study the commutation process of a newly designed pyro-breaker. Unlike normal circuit breakers, the arc discussed in this paper is discharged in deionized water. A parameter selection method is proposed. The practicability of the method is verified by numerical calculation in Power Systems Computer Aided Design (PSCAD) and experimentally.

Keywords: black-box arc model; DC circuit breaker; PSCAD; pyro-breaker

1. Introduction

1.1. Motivation and Incitement

Direct current (DC) power systems offer enhanced efficiency, reliability and simplicity over alternating current (AC) systems. They have been adopted in aircrafts, ships, urban transit systems and nuclear power plants [1–3]. Nonetheless, because there is no natural zero-crossing point, as in an AC system, extinguishing a DC arc is more challenging when it comes to avoiding breaking failure caused by the arc burning and reigniting [4].

Due to the fast responsiveness and highly reliability of pyro-breakers, they have been adopted as backup breakers in Quench Protection Systems (QPS) in a number of superconducting fusion facilities [5–9]. When a quench phenomenon occurs, the enormous electromagnetic energy in the superconducting coil is converted to heat energy [10]. This causes irreversible damage to the superconducting coil. Therefore, the energy needs to be commutated and consumed by a discharge resistor within a short period of time.

The pyro-breaker presented in this paper was developed from the concept of the pyro-breaker used in ITER [9] and it is expected that it will be utilized in an ongoing design project by the QPS for the China Fusion Engineering Test Reactor (CFETR) [11–13]. Various studies have been undertaken on the structure and thermal dynamics of the breaker [14,15]. As part of the design process, the breaker has to be tested in a high-power laboratory to confirm its performance and capability.
1.2. Literature Review

Arc models are a feasible way to study the commutation process theoretically and build on the tests results of a breaker. A fully developed arc model which has good correspondence with the arc behavior of the breaker can be applied to link the structural design to the commutation parameters of the pyro-breaker.

Research into DC arcs is usually conducted by means of dynamic arc models [16–18]. There are two types of dynamic arc model: the physical–mathematical model and the pure mathematical model. The physical–mathematical model describes arc characteristics by studying and analyzing the physical processes of the arc, which are very complex and difficult to measure. The pure mathematical model, i.e., the black-box model, treats the arc as an electrical component. It only describes the external relationship between the arc voltage and the arc current. Since Mayr and Cassie published their dynamic arc models [19,20], many studies have been devoted to studying and modifying their differential equations to fit the measured data [21–25]. Determining the values of the parameters of the arc model is considered to be the most difficult problem in the application of the black-box arc model. Furthermore, most of the existing arc model research has focused on arcs discharged in a vacuum or in open air [26–28]. The arc in the pyro-breaker presented here, however, is discharged in deionized water.

1.3. Paper Organization and Contribution

First, the structure of a pyro-breaker currently under design is introduced. Then the paper discusses the adoption of the Schavemaker black-box arc model, an improved Mayr-type arc model [23], to simulate the commutation process of the discussed pyro-breaker. It then discusses how the simulation was conducted, using Power Systems Computer Aided Design (PSCAD). Next, it describes how a fitted curve of the arc model parameter was obtained by examining ITER pyro-breaker tests. It then proposes a parameter selection method based on the fitted curve and verifies this on the newly designed pyro-breaker.

This method provides the theoretical basis for the study of the current commutation process of the pyro-breaker. It fills certain gaps in the literature regarding arc modeling in an underwater and explosive-driven circuit breaker, and provides a foundation for designing the pyro-breaker in QPS for CFETR.

2. Arc Modeling for Pyro-Breaker

2.1. The Commutation Section in the Pyro-Breaker

The commutation function is achieved through the Commutation Section (CS) in the pyro-breaker. As shown in Figure 1, the main components of the CS are the lower explosive, the support epoxy and the barrel conductor. The barrel conductor is a thin cylindrical copper wall. Circular grooves are arranged on the external surface to provide stress concentration, which leads to a high current density. Deionized water flows through the inner cavity of the barrel conductor and works as a cooling and detonation transmission medium. When the main breaker fails to disconnect the circuit, the CS is triggered to operate.

![Figure 1. Structure of the CS of the pyro-breaker: (1) upper conductor (2) deionized water (3) barrel conductor (4) support epoxy (5) explosive (6) lower conductor.](image-url)
After the detonation wave reaches the barrel conductor, the barrel conductor will break along the annular grooves. Due to the restrictions by the equidistantly installed support epoxy, the barrel conductor will break into several rings, as shown in Figure 2. Multiple arcs will appear between each ring and be extinguished by the high-pressure deionized water in the cylinder. The commutation capacity of the pyro-breaker depends on the number and size of the gaps between the rings. The current will commutate into a set of resistors to discharge the tremendous energy in the superconducting magnet. The arc behavior in the CS, which greatly affects the commutation capacity of the pyro-breaker, is determined by the structure and driving mechanism of the CS.

Figure 2. Formation of the barrel conductor in operation: (1) exterior epoxy (2) support epoxy (3) arc (4) explosive (5) barrel conductor (6) rings.

2.2. The Schavemaker Black-Box Arc Model

Black-box models describe non-linear arc conductance over time. The purpose of the black-box arc model is to study the external relationship between arc voltage and arc current during arc ignition.

The Mayr arc model, defined by Equation (1), and the Cassie arc model, defined by Equation (2), are the most widely used black-box arc models.

\[
\frac{1}{g} \frac{dg}{dt} = \frac{1}{\tau} \left( \frac{ui}{P_0} - 1 \right) \tag{1}
\]

\[
\frac{1}{g} \frac{dg}{dt} = \frac{1}{\tau} \left( \frac{u}{E_0} - 1 \right) \tag{2}
\]

Here, the time constant \(\tau\) shows the increasing rate of arc resistance. A smaller value of \(\tau\) indicates a shorter time for the arc resistance to reach a certain level. \(P_0\) is the cooling power, which depends on the internal characteristics of the circuit breaker. \(E_0\) is the reference arc voltage, which is irrelevant to the arc current. The Cassie and Mayr arc models are pure mathematical models, based on different assumptions. They both consider only one aspect of the heat dissipation equation. In fact, arc energy tends to dissipate in a manner that combines these two assumptions. In a circuit breaker, arc energy is mainly transmitted by convection and radial diffusion.

The Schavemaker black-box arc model, defined by Equation (3), is a Mayr-type arc model integrated with the Cassie arc model.

\[
\frac{1}{g} \frac{dg}{dt} = \frac{1}{\tau} \left( \frac{ui}{\max(E_0t, P_0 + P_1ut)} - 1 \right) \tag{3}
\]

\(P_1\) is the cooling constant, which adjusts the impact of the input power on \(P_0\). The pressure caused by ohmic heating during arc extinguishment is embodied in \(P_1\). In a high current area, Equation (3) is reduced to the Cassie arc model. Near the zero-current region,
Equation (3) is reduced to the Mayr arc model. The validity of both the Cassie model in a high current area and the Mayr model in a near-zero-current region have been proven.

As a result of the multiple gaps formed during the explosion in the CS, several arcs are ignited. To simplify the modeling, this series of arcs is regarded as a single arc.

3. Simulation and Experiment
3.1. Parameter Fitting

Schavemaker pointed out that the parameters in the equation can be either constant or a function of the electrical quantities. Many variations in these parameters can be found in [29]. Several of these varieties achieve good results in simulations. Schavemaker pointed out that there is no unique relationship between the electrical quantities and the parameters of the arc model. For example, at a certain time instant, \( k \), Equation (1) can be transformed to:

\[
\begin{bmatrix}
\frac{d\ln g}{dt} \\
ui_k \\
\tau_k \\
P_0_k
\end{bmatrix}
\begin{bmatrix}
l \n1 \\
i_k \n0
\end{bmatrix}
= 1 \text{ or } A\tilde{x} = b
\]  

Equation (4) is an under-determined system [30]. There are two unknown factors in one equation. It can be deduced that there is no unique set of \((\tau, P)\) values which can fit the current and voltage measured in the experiment. Hence, there is more than one set of parameter choices that can achieve a simulation which agrees with the actual switching characteristics.

Normally, the parameters of the black-box arc model are derived hypothetically and verified experimentally. A method to explore the parameter selection patterns is proposed here. The method adopts the Parameter Sweep Strategy [31,32] to fit the commutation test results of the ITER pyro-breaker in PSCAD.

The test circuit of the ITER pyro-breaker is illustrated in Figure 3. A current of sufficient amplitude was produced by means of capacitor bank \( C \). The ignition resistor \( R_i \) provided the necessary opening conditions for the ignitrons. After triggering the ignitrons, \( FV \), the current began to rise in the pyro-breaker branch. After the current reached the defined test level, the pyro-breaker operated and the current switched to the discharge resistor \( R \). The current pulse length and its value depended on the inductance of the coil, \( L \). The Rogowski coils, \( RC_1 \) and \( RC_2 \), were installed to measure the current in the pyro-breaker and the discharge resistor branches. A high-voltage probe was used to measure the voltage across the pyro-breaker.

![Figure 3. The test circuit of ITER pyro-breaker.](image)

The PSCAD model was built to simulate the test circuit of the ITER pyro-breaker, as shown in Figure 4. To simplify the simulation, a DC resource was selected as the power supply. Due to the characteristics of the electrical components, a resistor, \( R_1 \), was added to the inductance in the main circuit and an inductor, \( L_2 \), was added to the discharge resistor branch. The electrical parameters were set according to the ITER pyro-breaker test circuit, as shown in Table 1. The arc was regarded as a variable resistor, \( R_{arc} \). The module, \( R_{arc} \), was applied with the Schavemaker black-box arc model. \( I_{pb} \) is the current in the pyro-breaker branch. \( I \) is the current in the discharge resistor branch. \( V_{pb} \) is the voltage across the pyro-breaker. Since the resistance of the pyro-breaker was quite small, \( V_{pb} \) can be regarded as the arc voltage.
There are four parameters in the Schavemaker black-box arc model. \( E_0 \) is used to modify and calculate the value in the large current area. It has little influence on the current zero-crossing area. Hence, \( E_0 \) is set to 10 kV, according to the design requirements. For the values of \( \tau, P_0 \) and \( P_1 \), it can be concluded from the above analysis that there is no unique set of solutions to fit the arc model of the pyro-breaker. Schavemaker gave a set of parameter choices for an arc burning in SF\(_6\): \( \tau = 0.27 \mu s, P_0 = 15.917 \text{ kW} \) and \( P_1 = 0.9943 \). According to the definition of each parameter, the time constant, \( \tau \), in water should be smaller than the time constant in gas [33], while the cooling power, \( P_0 \), should be relatively larger than the cooling power in gas. Therefore, this study qualitatively selected a series of parameters in different orders of magnitude to run several simulations in PSCAD. It can be observed from the simulation results that as the time constant increased, the response time between arc ignition and breaking operation became longer. The cooling power, \( P_0 \), mostly affects the voltage waveform, and even a slight variation in \( P_1 \) has a significant effect on the time delay in arc ignition.

The oscillogram of the ITER pyro-breaker test at 72.5 kA is shown in Figure 5 [34]. As illustrated in Figure 5a, the commutation process began at 90 \( \mu\)s and finished at 199 \( \mu\)s, giving a total commutation time of 109 \( \mu\)s. The peak voltage was 14.9 kV, as shown in Figure 5b. In PSCAD, a set of simulations and parameter sweeping were conducted. Finally, a group of parameters that fit the test oscillogram was obtained, as illustrated in Figure 6. In the simulation, \( \tau \) was 0.02 \( \mu\)s, \( P_0 \) was 2500 kW and \( P_1 \) was 1.00147. The commutation time, the value and the time peak voltage occurred in the simulation agreed with the test results.
Based on the above analysis, $P_1$ is considered to be the only parameter affected by the input current among all four parameters. Hence, for pyro-breakers with the same driving mechanism, the value rule of $P_1$ under different input currents $I$ can be deduced. Based on this assumption, simulations and parameter fitting have been carried out for a large number of ITER pyro-breaker tests [34–37] and the $P_1$-$I$ diagram, illustrated in Figure 7, obtained.

By examining the $P_1$-$I$ diagram, it can be observed that the value of the parameter $P_1$ has a linear relationship with the input current defined by Equation (5). The fit goodness ($R^2$) is 0.98383.

$$P_1 = 2.374 \times 10^{-5} I + 0.9997 \quad (5)$$

It needs to be mentioned that a pyro-breaker is a single-action switch with a very fast and transient operation process driven by explosives. It is necessary to reassemble the breaker and reconnect it into the circuit after each test, which may alter the stray inductance value of the circuit. This can lead to differences in the commutation process under the same current. Therefore, the data obtained from several tests at the same current were averaged and any highly inconsistent datapoints were deleted.

### 3.2. Simulation and Experiment

The test model illustrated in Figure 4 was also applied to simulate the commutation process of the pyro-breaker designed for CFETR, in order to verify the proposed value rule of $P_1$. As shown in Table 2, the electrical parameters were set according to the test circuit: $P_0 = 2500$ kW, $\tau = 0.02$ $\mu$s and $E_0 = 2$ kV, according to the design requirements. Based on Equation (5), when the input current is 40 kA, $P_1$ is 1.0006.
Table 2. The electrical parameters in the CFETR pyro-breaker test circuit.

| Electrical Components | $L_1$ | $R_1$ | $L_2$ | $R_2$ |
|-----------------------|-------|-------|-------|-------|
| Value                 | 5 mH  | 2.5 mΩ| 20 µH | 50 mΩ |

The simulation results are shown in Figure 8. Due to the setting of a delay, the current in the pyro-breaker branch began to commutate to the resistance branch from 200 µs. Simultaneously, the voltage across the breaker, i.e., the arc voltage, began to increase. The current in the pyro-breaker branch crossed the zero point at 413 µs. The arc voltage reached a peak value of 9.20 kV at 346 µs.

![Figure 8](image)

Figure 8. Simulation results in PSCAD of the CFETR pyro-breaker at 40 kA: (a) current oscillogram; (b) voltage oscillogram.

The commutation test of the pyro-breaker was carried out on a DC test platform. The output current of the platform was set to 40 kA. The test circuit is illustrated in Figure 9. The inductance of the discharge resistor branch was 20 µH. The resistance of the inductance was 2.5 mΩ. Two Rogowski coils were installed in the pyro-breaker branch and the discharge resistor branch to measure the current. A voltage differential probe was applied to measure the voltage across the breaker.

![Figure 9](image)

Figure 9. The test circuit of the CFETR pyro-breaker.
The oscillograms of the commutation test are shown in Figure 10. The current in the pyro-breaker branch began to commutate at 100 µs and finished at 321 µs. The current commutating speed reached its peak value at around 240 µs. This lead to a large $\frac{di}{dt}$ and resulted in the appearance of a peak voltage of 9.17 kV.

Figure 10. CFETR pyro-breaker tested at 40 kA: (a) current oscillogram; (b) voltage oscillogram.

3.3. Discussion

The application of black-box arc models in a circuit breaker is very complicated, especially when the arc is discharged underwater. The selection of parameters is the main problem. There are four parameters in the Schavemaker black-box arc model: the time constant, the cooling power, the cooling constant and the reference voltage constant. Based on a set of parameter choices given by Schavemaker, curve fitting for the ITER pyro-breaker was performed using the parameter sweep strategy. As illustrated in Figures 5 and 6, the simulation in PASCAD corresponded well with the test results.

By analyzing the sweeping process and the simulations, it can be concluded that as the time constant increased, commutation duration became longer and the peak current became higher. The cooling power had the same effects as the reference voltage. They mostly affected the voltage waveform. As the cooling power increased, the voltage diagram changed into a sharp-shaped waveform. The cooling constant was the only parameter affected by the input current among all four parameters. As shown in Figure 7, within an input current range of 70–90 kA, the change in $P_1$ was within $5 \times 10^{-4}$. Even a slight variation in $P_1$ had a significant effect on the time delay of the arc ignition. This might be because the model was applied in a high-power situation. The influence of the electrical power input was relatively higher than in the lower input power situation. Moreover, the stray inductance value of the circuit varies every time the pyro-breaker is reassembled and connected into the circuit, leading to differences in the commutation process under the same current. Any analysis of the relationship between $P_1$ and the input current needs take this variation into account.

As shown in Figure 8a, the commutation time was 213 µs and the commutation speed reached its highest value at 146 µs in the simulation results. As shown in Figure 10a, the commutation time was 221 µs and the commutation speed reached its highest value at 140 µs in the experimental results. By comparing the results of the simulation and the experiment, it can be concluded that the current commutation time and the peak voltage obtained from the simulation agree with the experimental results. It can be inferred that the values for $(P_0, \tau$ and $E_0)$ determined in this paper can be applied in pyro-breakers with a similar driving mechanism, and that $P_1$ can be determined by the proposed method under different input currents.
It can be observed from Figure 10a that the current curve of $I_r$ has a small hump in the beginning section of the commutation phase. This might because multiple gaps are formed at different speeds during the explosion. This would result in a certain randomness in the rate of change of the arc resistance and the arc voltage. As illustrated in Figure 8b, the simulated voltage has a smoother waveform than the voltage waveform of the test illustrated in Figure 10b. For modelling purposes, in this paper the multiple arcs were regarded as a single arc. In future simulations, this randomness could be treated as a factor of the arc model to enhance the accuracy of the simulation.

4. Conclusions

The arc, as an inevitable phenomenon occurring when a direct current (DC) circuit breaker is opened, directly determines the performance of the breaker. It is very challenging to develop a pure physical model based on arc characteristics. Many studies have focused on the application of the black-box arc model in the analysis of arc behavior in circuit breakers. Nevertheless, the application of the black-box arc model for this type of breaker, in which the arc ignites under water, remains to be explored.

The Schavemaker arc black-box model was applied to study the current commutation of the presented pyro-breaker. By analyzing the test results of the pyro-breaker in ITER, a suitable method for the selection of parameters was proposed. The feasibility of this method was verified by means of experiments on the pyro-breaker prototype designed for the China Fusion Engineering Test Reactor (CFETR), which was developed from the concept of the pyro-breaker used in ITER. This method provided a theoretical basis for the study of the current commutation process of the pyro-breaker.

Since the pyro-breaker presented here is an extremely fast, nonlinear and single-operated switch, it is necessary to build a more accurate and stable test platform to measure the commutation process. A high-speed camera could be implemented into the platform to inspect the arc’s behavior during the operation. Also, the randomness in the gap formation of the commutation section (CS) should be factored into the arc modeling to enhance the accuracy of the simulation. The operation time is extremely short, so contamination of the deionized water was ignored in this paper. However, changes in the electrical characteristics of the water and their effect on arc ignition could be valuable future research directions. Moreover, for this kind of complex problem, Artificial Intelligence techniques could be considered for parameter fitting in the future.

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Nomenclature of the Variables

- $g$: arc conductance
- $t$: time
- $u$: arc voltage
- $i$: arc current
- $\tau$: time constant
- $P_0$: cooling power
- $E_0$: reference arc voltage
- $P_1$: cooling constant
- $I_{pb}$: current in the pyro-breaker branch
- $I_r$: current in the discharge resistor branch
- $V_{pb}$: voltage across the pyro-breaker
- $R^2$: fit goodness

Abbreviations

- DC: direct current
- AC: alternating current
- QPS: Quench Protection System
- ITER: International Thermonuclear Experimental Reactor
- CFETR: China Fusion Engineering Test Reactor
- PSCAD: Power Systems Computer Aided Design
- CS: Commutation Section

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