At the beginning of the 20th century, the use of radio waves caused the genesis of the wireless communications era. Soon after, the same radio waves contributed to revolutionizing navigation. In this way, the era of radio-navigation began. Its origins are mainly hyperbolic terrestrial navigation systems (TNSs). For this type of systems, we can include the Decca Navigator System, Consol, Omega, Syledis, Loran-A, Loran-C, Chayka, and Jemioluska [1–6]. The TNSs were mainly used in sea and air transport. In addition, ground-based augmentation systems (GBASs) were developed mainly for aviation, e.g., the ILS, MLS, DME, VOR, and TACAN [7].

In the late 1970s, the United States developed the first navigation satellite system (NSS), i.e., the Transit, also known as the Navy NSS or NAVSAT [5]. The positioning in the Transit was based on the Doppler effect. His successor is the GPS–NAVSTAR (Global Positioning System – Navigation Signal Timing and Ranging), i.e., the first global NSS (GNSS), which is widely used in civil applications [1,8,9]. At present, the GNSSs have dominated determining the position and direction of objects’ movement in both air, sea, and land transport. The Russian GLONASS and European Galileo are also counted among the GNSSs [1,8,9]. In addition, regional NSSs (RNSSs) are available in certain regions of the world, including the Chinese BeiDou (BDS), Japanese QZSS, Indian NAVIC [1,8,9]. From 2020, the BDS will gain the status of the global system. Positioning in the GNSSs and RNSSs is based on time of arrival (TOA) measurements and a multilateration method, popularly known as a time difference of arrival (TDOA) [10]. In this case, a point localization in space using the TDOA requires receiving a signal from at
least four satellites of the NSS. This method is the basis of most hyperbolic systems, including the TNs. Additionally, the GNSSs and RNSSs use code-division multiple access (CDMA) technique, with the exception of the GLONASS, which is based on frequency-division multiple access (FDMA) [9]. Satellite-based augmentation systems (SBAs) [1,8,9] are widely used in aviation and also in maritime [11]. To the SBAs, we may include, i.a., the American WAAS, European EGNOS, Japanese MSAS, Indian GAGAN, Russian SDMC, and Chinese SNAS. For supporting systems, the French DORIS (Doppler Orbitography and Radio-positioning Integrated by Satellite) is also included [12]. This system based on the Doppler effect ensures high positioning accuracy.

A space segment is an essential part of all satellite systems. In that, the availability of the system over a whole or major area of the Earth is assured. However, this issue causes the costs of implementing and maintaining such systems are very high. Most of the GNSSs and RNSSs are military systems with the possibility of commercial civil applications. The Galileo and QZSS are only civilian systems. The availability of receiving devices, coverage for the NSSs, and high positioning precision in relation to the TNs caused that at the end of the 20th century, most of the TNs ceased to be supported and operated. While the GBASs are still used. Currently, the eLoran is the only operating TNS [13,14]. It consists of about forty stations located mainly along the coasts of the United States, the European Union, and Southeast Asia. This provides coverage for the northern parts of the Indian, Pacific, and Atlantic Oceans.

Over the past thirty years, we have been observing the rapid development of the GNSSs. At the same time, the development of mobile cellular networks has provided access to cheap and universal GPS receivers in smartphones. These two aspects have resulted in the dissemination of the satellite navigation and location-based services (LBSs) [15], especially in civilian land traffic. On the other hand, the widespread use of the NSSs is a secondary reason for reducing the security of countries that do not have their own NSS, as well as those that provide such the system. Lowering safety results from several premises. First, the military GNSS administrator may cause the signal to be turned off or decreasing the positioning accuracy for civilians in a specific area, e.g., military operations. In this case, military users can use code signals unavailable to civilians. Secondly, elements of the ground control or space segments may be destroyed by the enemy. Thirdly, at the last time, dynamic development of jamming and spoofing techniques dedicated to the GNSS is observed [16–19]. In this case, the use of the satellite navigation may be impossible or cause false results. The second and third reasons are a serious threat to military systems, including those countries that have own GNSS or RNSS. On the other hand, the aforementioned development of GNSSs resulted in the break of the support and development of alternative positioning methods, such as the TNs.

In recent years, the development of the new TNs is again considered seriously by many countries, especially for army needs in a period and area of military operations. For example, in 2012, the Armament Inspectorate of the Polish Ministry of Defense resumed an analytical-conceptual phase in development terms of “The medium-range radio-navigation system for the Polish Navy” [20]. The result of these activities is the “The medium-range mobile radio-navigation system” developed currently by the Research and Development Center for Maritime Technology [21]. This system will be based on the effects of a research team from the Gdansk University of Technology. This team has developed the TDOA-based asynchronous and self-organizing navigation system called the AEGIR [22–24]. The work undertaken by the NATO Science & Technology Organization (STO) and the European Defense Agency in the area of “Navigation in GNSS denied environment” is another premise in this direction [25–27]. However, a monitoring system of own combat units’ location named the blue force tracking (BFT) [28–31] belongs to the priorities of modernization of the Polish Army. In this case, the positioning the soldiers, equipment, and units of own forces in the absence of the GNSS access is also considered.

In 2016, a proposal to use a coastal radio-beacon (RB) system and the signal Doppler frequency (SDF) location method for positioning ships in a coastal zone was presented [20]. The SDF method [32–34], like the previously mentioned Transit and DORIS, as well as the COSPAS-SARSAT [35,36], a satellite system used in search and rescue (SAR) operations, are based on the Doppler effect. In [20], the results of simulation studies for scenarios in the Baltic Sea are presented. The use of the stationary RBs is a good solution in peacetime. However, in the case of the military operations, the reserved radio-navigation system should base on mobile RBs. The purpose of this paper is to present the concept of a mobile reserve navigation system (MRNS) for ships in the coastal zone. The effectiveness of vessel positioning using the developed system is presented based on simulation studies.

The remainder of the paper is organized as follows. In Section 2, the characteristics of the transmitting and receiving parts of the MRNS and the SDF method are presented. Section 3 contains a description of a scenario and assumptions for simulation studies. The simulation results illustrating the accuracy of the ship positioning are shown in Section 4. The paper is finished with final remarks and a summary.

2 MOBILE RESERVED NAVIGATION SYSTEM

2.1 System Concept

In general, the concept of the MRNS is based on the assumptions of the stationary reserved TNS for ships, which are presented in [20], i.e.,

- the system consists of several or dozen RBs operating in an asynchronous broadcasting mode,
- multi-antenna and multi-frequency-channel receiving system located on the ship enables simultaneous analysis of signals from the several RBs,
- the SDF is used to determine the position of the ship, i.e., the position of a reference receiving antenna on this ship.
The significant differences between the stationary and mobile versions mainly concern the transmitting part of the system. Stationary beacons are the core of the system presented in [20]. Their deployment was planned in existing coastal infrastructure. Considering propagation properties of radio waves, we proposed using lighthouses as points located high above sea level. In the MRNS, the RBs are placed on vehicles that can change position. Each new position brings changes in the transmitting signal.

A detailed description of the mobile RB is presented in Section 2.2. The receiving part of the system located on the ship is described in Section 2.3. In Section 2.4, the SDF implementation method in the receiving part of the MRNS is contained.

2.2 Transmitting part of system

The transmitting part of the MRNS consists of $K$ mobile RBs. The concept of the RB is depicted in Figure 1.

The main components of the transmitting part are identical to those in the stationary version of the RB [20], i.e., the transmitting antenna, power amplifier, and signal generator.

The generator should be made in the software-defined radio (SDR) technology [37–39] in order to be able to transmit different signal structures (waveforms). In this case, emitting the current position of the RB is important. In the stationary system, the RB transmits one type of the signal because its position is fixed. The microcomputer connected to the SDR transmitter provides the ability to generate the broadcasting signals with information about the current position of the RB.

The RB devices are placed on board a wheeled vehicle. The proposed MRNS is based on the Doppler effect. Therefore, the frequency stability of each signal source is very important [40]. Hence, we suggest equipping each RB with a rubidium or cesium frequency standard.

In order to ensure a larger operation range of the RB, each vehicle should be equipped with a hydraulic or pneumatic telescopic (locking) mast. These masts allow increasing the antenna height up to 50 m. Therefore, the vehicle should be also equipped with hydraulic stabilizers using in technical vehicles. The stabilizers are necessary to ensure stable operation of the mobile RB in different weather conditions, e.g., strong wind, stormy weather, etc. A time of assembly and disassembly of the antenna mast should be as short as possible, which will allow for a quick change of the vehicle location.

Knowing the exact position of the RB is essential for its proper operation. Hence, the identification of potential points on the coast, from which the RB may transmit the signal, is required. At such points, averaged position measurements using the GNSS should be performed in the peacetime. In the field, appropriate marking of these points should be introduced, e.g., similar to geodetic reference points (benchmarks). This point may explicitly give geographic coordinates, e.g., on a nameplate or only a benchmark number associated with the coordinates in the system. This approach allows the use of the mobile RBs in GNSS-denied conditions.

In addition, the RB should be equipped with a GNSS receiver to operate in availability conditions of the GNSS signal. We may imagine a scenario of using the MRNS when the GNSS is available on land and jamming or spoofing at a sea. In this case, the RB may emit the signals from any unmarked point on the coast. Then, the GNSS receiver should be connected to the SDR generator via the microcomputer. The GNSS receiver antenna should be placed outside the vehicle and an application that controls the waveform generation should provide an appropriate coordinate conversion between the GNSS and RB antennas.

In addition to an onboard power supply of the RB components, the vehicle should be equipped with a backup power source, e.g., an engine generator and uninterruptible power supply (UPS).

In [20], we assumed that individual RBs transmit phase-shift keying (PSK) signals. The location methodology of a PSK signal source using the SDF is presented in [41].

2.3 Receiving part of system

The receiving part of the MRSN is not changed compared to the stationary system presented in [20]. In Figure 2, an exemplary arrangement of the receiving antennas (RAs) on the shipboard is illustrated.

RA is the reference antenna to which the ship position is determined in the MRNS. From the viewpoint of the ship antenna system, the proposed solution works in the multi-input-multi-output (MIMO) or single-input-multi-output (SIMO) mode for the vessel positioning based on multiple RBs or only one, respectively.

The receiver in the MRSN is a multi-channel device. On the one hand, this means that the signals from $J$ RAs are fed to the receiver. On the other hand, each signal supplied from the $j$th RA ($j = 1, 2, \ldots, J$) contains the signals from $K$ RBs that operate on $K$ frequency sub-bands (channels). For this reason, the receiver is made in the SDR technology [37–39].
Signal processing carries out in parallel using a multi-threaded application. The signal from each antenna is divided into frequency sub-bands. For this purpose, digital filtration is carried out. In each sub-band, the information about the RB position is decoded and a Doppler frequency shift (DFS) of the received signal is determined. For each RB, estimated DFS changes versus time, so-called the Doppler curve, is obtained by averaging and transforming (5) \[20\]. In this case, a change of the object movement direction is required.

In a navigation application based on the SDF, in the first step, the coordinates of the RBs are determined in the local coordinate system associated with Rx. In the second step, the estimated coordinates of the RBs are referenced to the actual positions obtained in the received signal. On this basis, the Rx (ship) position is determined.

From the technical viewpoint, two parameters, \(\Delta T\) and \(T_\alpha\), are significant. \(\Delta T\) is the analysis time of the received signal which is used to determine the instantaneous DFS. Whereas, \(T_\alpha\) is the averaging time of the Doppler curve, which is used to estimate the localized-object coordinates, i.e., the RB. Therefore, estimation of the RB position is based on \(N\) discrete instantaneous values of the DFSs, \(f_{DL_{k,j}}(t)\), for each RB.

\[
N = \left| \frac{T_\alpha}{\Delta T} \right| \tag{4}
\]

The ship coordinates are calculated in the same way as in \[20\]. For each \(k\) and \(j\) \((k = 1, 2, ..., K, j = 1, 2, ..., J)\), the set of the DFSs \(f_{DL_{k,j}}(t)\) \((n = 1, 2, ..., N)\), creates the Doppler curve. For the positioning of each RB, the SDF uses (2) and fragments of these Doppler curves. For \(TA_\alpha\) and each \(i\)th antenna-channel (RA) of the Rx, the position of the \(k\)th RB is determined as follow \[20\]

\[
x_{RB_{k,j}} = \sqrt{\sum_{i=1}^{n} \left( t_i A_{k,j}(t_i) - t_i A_{k,j}(t_j) \right)^2 + \left( t_i - t_j \right) A_{k,j}(t_i) A_{k,j}(t_j)} - z_0
\]

\[
y_{RB_{k,j}} = \pm \sqrt{\frac{(t_i - t_j) A_{k,j}(t_i) A_{k,j}(t_j)}{A_{k,j}(t_i) - A_{k,j}(t_j)}} - \overline{z_{RB_{k,j}}}
\]

\[
z_{RB_{k,j}} = z_{0RB_{k,j}} - z_0 - z_{RA_{k,j}} \tag{5}
\]

where

\[
A(t) = \frac{\sqrt{F(t)} - \bar{f}_D(t)}{F(t)} \quad F(t) = \frac{\bar{f}_D(t)}{f_{DL_{max}}}
\]

\[6\]

\[
A_{k,j}(t) = \sqrt{1 - \frac{F_{k,j}(t)}{F_{DL_{max}}}} \quad F_{k,j}(t) = \frac{f_{DL_{k,j}}(t)}{f_{DL_{max}}}
\]

and \(f_{DL_{max}} = f_0 v / c\); \(f_0\) is the carrier frequency of the \(k\)th RB.

Based on the \(k\)th RB signal, the vessel position is obtained by averaging and transforming (5) \[20\].
\[
x_k = \left(\sum_{j=1}^{J} x_{RB,j} + x_{RA}\right) \cos \alpha \\
+ \left(\sum_{j=1}^{J} y_{RB,j} + y_{RA}\right) \sin \alpha + x_{0RB} \\
y_k = -\left(\sum_{j=1}^{J} x_{RB,j} + x_{RA}\right) \sin \alpha \\
+ \left(\sum_{j=1}^{J} y_{RB,j} + y_{RA}\right) \cos \alpha + y_{0RB} \\
z_k = z_{0RB} - \left(\sum_{j=1}^{J} z_{RB,j} + z_{RA}\right) = z_0
\]

where \(\alpha = 90^\circ - \beta\); and \(\beta = \) the direction of the ship movement relative to the North.

If the Rx uses only the signal from a single RB, then the current position of the ship is \((x, y, z) = (x_k, y_k, z_k)\). If the Rx receives the signals from more than one RB, the averaging process of the ship position is additionally executed. In this case, for \(K\) analyzed RBs, the weighted-mean algorithm is used

\[
(x, y, z) = \frac{1}{W} \left(\sum_{k=1}^{K} w_k x_k, \sum_{k=1}^{K} w_k y_k, \sum_{k=1}^{K} w_k z_k\right)
\]

where

\[
w_k = 1 - \left|\frac{1}{J} \sum_{j=1}^{J} F_{k,j}(t)\right| \quad \text{and} \quad W = \sum_{k=1}^{K} w_k
\]

The proposed averaging algorithm considers the Doppler curve shapes and is more accurate than an arithmetic-mean [43].

### 3 SCENARIO AND ASSUMPTIONS FOR SIMULATION STUDIES

Simulation studies are carried out for the spatial scenario shown in Figure 3. In this case, we assumed that three RBs, marked as RB1, RB2, and RB3, are located on a shore of the Baltic Sea in localities of Łazy, Darłowo, and Jarosławiec, respectively. The position coordinates in WGS 84 and UMT for these RBs and three points, i.e., P1, P2, and P3, which determine two measurement routes, P1→P2 and P1→P3, are included in Table 1.

| Point | WGS 84 Latitude (° N) | Longitude (° E) | UMT Northing (m N) | Easting (m E) |
|-------|------------------------|-----------------|-------------------|--------------|
| RB1   | 54.308662              | 16.201313       | 6018530           | 578160       |
| RB2   | 54.432433              | 16.377603       | 6032510           | 589360       |
| RB3   | 54.535533              | 16.540890       | 6044200           | 599700       |
| P1    | 54.531990              | 15.867716       | 6043060           | 556150       |
| P2    | 54.331924              | 16.028052       | 6020940           | 566850       |
| P3    | 54.594149              | 16.553212       | 6050739           | 600353       |

![Figure 3. Spatial scenario for simulation studies (based on Google Earth Pro)](image)

As described in Section 2.1, each RB is equipped with the telescopic mast. In simulations, the mast height is equal 50 m. For simplicity, we assumed that each vehicle with the RB is located 10 m above sea level. Hence, for all RBs, the identical antenna height is defined, i.e., \(h_{RA} = 60\) m. Location of RAs on the ship was assumed as in Figure 2, according to the assumptions shown in [20]. Assuming that the height of the lowest located RAs, i.e., for RA5 and RA6, is \(h_{RA} = 11\) m above sea level, then a radio horizon for each RB is about 45 km. Therefore, line-of-sight (LOS) conditions are provided in every point on two analyzed measurement routes.

Other assumptions for simulation studies are similar to shown in [20]. The RBs transmit PSK signals with bandwidth \(B = 200\) kHz at frequencies \(f_0 = 1860\) MHz, \(f_2 = 1860.3\) MHz, and \(f_3 = 1860.6\) MHz, respectively for RB1, RB2, and RB3. On the frequencies \(f_0 + 0.75B\), \(k = 1, 2, 3\), the pilot signal used in the SDF is additionally transmitted. The minimum carrier-to-noise ratio is \(CNR_{\text{min}} = 5\) dB. The basic frequency of the spectral analysis is 1 mHz. Additionally, we adopted \(\Delta T = 1\) s and \(T_A = 240\) s. The speed of the ship relative to land is \(v = 20\) w. \(\cong 10.3\) m/s.

### 4 RESULTS OF SIMULATION STUDIES

The purpose of the carried out simulation tests is to assess the positioning accuracy and to present several aspects of the SDF use in the MRNS. In Section 4.1, the comparison of the arithmetic and weighted averaging the ship coordinates is shown. This analysis is based on the results obtained for the measurement route P1→P2. Section 4.2 contains a comparison of the...
positioning results at two considered measurement routes.

The basic measure of positioning accuracy is the position error defined as follows [33]

$$\Delta R = \sqrt{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2}$$  \hspace{1cm} (10)

where \((x, y, z)\) and \((x, y, z)\) = the estimated and real coordinates of the vessel, respectively.

4.1 Comparison of arithmetic and weighted averaging

The simulation studies are carried out for the measuring route P1→P2 and the assumptions described in Section 3. Figures 4 and 5 show the ship position at the route based on the arithmetic and weighted averaging, respectively. Additionally, average position errors for the entire route are marked with dashed lines.

In order to assess the qualitative positioning of the ship using the two analyzed averaging methods, a cumulative distribution function (CDF) is determined for the position error, \(F(\Delta R)\). These CDFs are illustrated in Figure 6. The results obtained confirm the greater accuracy of estimating the ship position using the weighted average.

4.2 Comparison of ship positioning at different measurement routes

The two measurement routes shown in Figure 3 differ in their location relative to three analyzed RBs. This transfers into other Doppler curves for three RBs obtained in the ship receiver at the individual measurement routes. Changes of the theoretical DFSs calculated based on (1) are depicted in Figures 7 and 8 for the routes P1→P2 and P1→P3, respectively.

Based on the shown Doppler curves, we can see that the DFSs changes are more diverse for the route...
P1→P2. Using the weighted average in the SDF reduces the impact of the DFS variability on the positioning accuracy.

In Figure 9, the vessel position error along its movement trajectory at the route P1→P3 for the weighted average is illustrated. Analogous results for the route P1→P2 are depicted in Figure 5.

![Figure 9. Ship position error at route P1→P3 using weighted averaging](image)

Due to the weighted average, the results obtained for both routes are similar. In this case, the average error for the entire route is equal to 19.5 m. This is also clearly visible in the CDF graphs shown in Figure 10.

![Figure 10. CDFs for two analyzed routes](image)

The obtained results coincide with those presented for the stationary backup system [20].

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