On Low-Complexity Decoding of Product Codes for High-Throughput Fiber-Optic Systems

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(Invited Paper)

Abstract—We study low-complexity iterative decoding algorithms for product codes. We revisit two algorithms recently proposed by the authors based on bounded distance decoding (BDD) of the component codes that improve the performance of conventional iterative BDD (iBDD). We then propose a novel decoding algorithm that is based on generalized minimum distance decoding of the component codes. The proposed algorithm closes over 50% of the performance gap between iBDD and turbo product decoding (TPD) based on the Chase–Pyndiah algorithm. Moreover, the algorithm only leads to a limited increase in complexity with respect to iBDD and has significantly lower complexity than TPD. The studied algorithms are particularly interesting for high-throughput fiber-optic communications.

I. INTRODUCTION

The advent of codes-on-graphs and advances in digital electronics have spurred a great deal of research on soft-decision forward error correction (SD-FEC) for fiber-optic communications in the last decade, see, e.g., [1]–[5] and references therein. Contrary to other applications such as wireless communications—where SD-FEC is the de-facto standard—research on SD-FEC in fiber-optic communications has been paralleled by a revival of research on hard-decision FEC (HD-FEC). The reason is that SD-FEC entails a significantly higher decoding complexity and data flow compared to HD-FEC. Thus, for applications where very high throughputs and low power consumption are required, HD-FEC is still an appealing alternative. HD-FEC can also be combined with multilevel modulation formats to achieve high spectral efficiency [6]–[8].

Recent research on HD-FEC for fiber-optic communications has been largely fuelled by the proposal of several new classes of product-like codes, such as staircase codes [9] and braided codes [10], [11], which we refer to as generalized product codes (GPCs). Similar to the original product codes (PCs) [12], GPCs are built from smaller component codes, typically Reed–Solomon or Bose–Chaudhuri–Hocquenghem (BCH) codes, which can be efficiently decoded via algebraic bounded distance decoding (BDD). The overall GPC can then be decoded by iteratively applying BDD to the component codes. This algorithm is referred to as iterative BDD (iBDD) and achieves an excellent performance–complexity trade-off.

GPCs can also be decoded iteratively by employing soft-input soft-output (SISO) component decoding. This is referred to as turbo product decoding (TPD) and typically implemented in practice via the Chase–Pyndiah algorithm [13]. TPD yields larger net coding gains than iBDD but it has a significantly higher decoding complexity. In order to (roughly) quantify the complexity increase, one may rely for example on decoder data flow considerations [9] or compare existing implementations (e.g., [14], [15]) in terms of gate counts. Both approaches reveal that the complexity and potential power consumption increases by around 1–2 orders of magnitude when switching from iBDD to TPD. Given that commercially available implementations of TPD already consume around 8 W to achieve a throughput of 100 Gb/s [15], it remains a significant challenge to scale the larger net coding gains to even higher throughputs. On the other hand, staircase decoders based on iBDD remain feasible for throughputs as large as 1 Tb/s [16].

The recent years have seen an increasing interest in the research community in closing the gap between the performance of HD-FEC and SD-FEC, while keeping the decoding complexity low. An interesting line of research is to concatenate an inner SD-FEC code, e.g., a low-density parity-check (LDPC) code decoded via belief propagation, with an outer staircase code [4], [5]. Another alternative, investigated by the authors in [17] and [18], is to improve the performance of iBDD. In [17], a new anchor decoding (AD) algorithm that exploits conflicts between component codes in order to assess their reliabilities, even when no channel reliability information is available, is proposed. The algorithm in [18] improves performance by exploiting channel reliabilities, while still only exchanging binary (hard-decision) messages between component codes, similar to iBDD.2

1TPD can also be based on other component decoders, e.g., the forward-backward algorithm applied to the component code trellis. In this paper, we use the term TPD to refer to the iterative SISO decoding based on the Chase–Pyndiah algorithm.

2A similar approach was analyzed in the context of low-complexity decoding algorithms for LDPC codes in [19].
In this paper, we study and compare several decoding algorithms for GPCs based on algebraic decoding of the component codes. Our focus is on PCs, but the considered algorithms can also be applied to GPCs such as staircase and braided codes. We start by reviewing the two decoding algorithms that were proposed in [17] and [18], respectively. It is shown that for the considered scenario, both algorithms offer sizable net coding gain improvements of 0.18 dB and 0.25 dB, respectively, with only a small complexity increase compared to iBDD. We then propose a novel iterative decoding algorithm based on generalized minimum distance (GMD) decoding of the component codes, which we refer to as iterative GMD decoding with scaled reliability (iGMDD-SR). Using iGMDDDR-SR, a more significant coding gain improvement of around 0.60 dB can be achieved compared to iBDD. This closes over 50% of the performance gap to TD, while maintaining significantly lower complexity.

Notation: We use boldface letters to denote vectors $x$ and matrices $X = [x_{i,j}]$. The $i$-th row and $j$-th column of $X$ are denoted by $X_{i,:}$ and $X_{:,j}$, respectively. $|a|$ denotes the absolute value of $a$, and $\lfloor a \rfloor$ the maximum integer value less than or equal to $a$. $\mathcal{N}(\mu, \sigma^2)$ represents a Gaussian distribution with mean $\mu$ and variance $\sigma^2$. The Hamming distance between vectors $a$ and $b$ is denoted by $d_H(a, b)$.

II. PRELIMINARIES

Let $C$ be a binary linear $(n, k, d_{\text{min}})$ code, where $n$, $k$, and $d_{\text{min}}$ are the code length, dimension, and minimum distance, respectively. A (two-dimensional) PC with parameters $(n^2, k^2, d_{\text{min}}^2)$ and rate $R = k^2/n^2$ is defined as the set of all $n \times n$ arrays such that each row and column of the array is a codeword of $C$. Accordingly, a codeword of the product code can be represented as a binary matrix $C = [c_{i,j}]$ of size $n^2 \times n^2$. Alternatively, a PC can be defined via a Tanner graph with $2n$ constraint nodes (CNs), where $n$ CNs correspond to the row codes and $n$ CNs correspond to the column codes. The graph has $n^2$ variable nodes (VNs) corresponding to the $n^2$ code bits. The code array and (simplified) Tanner graph of a PC where $n = 6$ is shown in Fig. 1.

We assume transmission over the binary-input additive white Gaussian noise (bi-AWGN) channel. In particular, the channel observation corresponding to code bit $c_{i,j}$ is given by

$$y_{i,j} = x_{i,j} + z_{i,j},$$

where $x_{i,j} = (-1)^{c_{i,j}}$ and $z_{i,j} \sim \mathcal{N}(0, (2RE_b/N_0)^{-1})$. Let $L = [L_{i,j}]$ be the matrix of channel log-likelihood ratios (LLRs) and $R = [r_{i,j}]$ the matrix of hard decisions at the channel output, where $r_{i,j}$ is obtained by mapping the sign of $L_{i,j}$ according to $-1 \to 0$, $+1 \to 1$. This mapping is denoted by $B(\cdot)$, i.e., $r_{i,j} = B(L_{i,j})$. With some abuse of notation, we also write $R = B(L)$.

A. Bounded Distance Decoding

Consider now the decoding of an arbitrary row or column component code, assuming that the codeword $c = (c_1, \ldots, c_n)$ is transmitted and only hard-detected channel observations $r = (r_1, \ldots, r_n)$ are available. BDD corrects all error patterns with Hamming weight up to the error-correcting capability $t = \left\lfloor \frac{d_{\text{min}} - 1}{2} \right\rfloor$ of the code. If the weight of the error pattern is larger than $t$ and there exists another codeword $\hat{c} \in C$ with $d_H(\hat{c}, r) \leq t$, then BDD maps $r$ to $\hat{c}$ and thus introduces a miscorrection. Otherwise, if no such codeword exists, BDD fails and we use the convention that the decoder outputs $\hat{r}$. Thus, the decoded vector $\hat{r}$ for BDD can be written as

$$\hat{r} = \begin{cases} c & \text{if } d_H(c, r) \leq t \\ \hat{c} \in C & \text{if } d_H(c, r) > t \text{ and } d_H(\hat{c}, r) \leq t \\ r & \text{otherwise} \end{cases}.$$

B. Generalized Minimum Distance Decoding

Consider again the component decoding but now assume that the vector of channel LLRs $l = (L_1, \ldots, L_n)$ is available. In that case, GMD decoding can be employed which is based on multiple algebraic error-erasure decoding attempts [20]. In particular, the decoder ranks the coded bits in terms of their reliabilities $|L_1|, \ldots, |L_n|$. Then, the $m$ least reliable bits in $r$ are erased, where $m \in \{d_{\text{min}} - 1, d_{\text{min}} - 3, \ldots, 2\}$ if $d_{\text{min}}$ is odd and $m \in \{d_{\text{min}} - 1, d_{\text{min}} - 3, \ldots, 3\}$ if $d_{\text{min}}$ is even. Together with $r$, this gives a list of $t + 1$ trial vectors $\tilde{r}_i$, out of which $t$ vectors contain both erasures and (possibly) errors. Finally, algebraic error-erasure decoding [21, Sec. 6.6] is applied to each $\tilde{r}_i$, $i = 1, \ldots, t + 1$. If error-erasure decoding fails for all $t + 1$ vectors in the list, an overall failure is declared for the GMD decoding. On the other hand, if some of the error-erasure decoding attempts did not fail, the decoder picks among all decoded candidate codewords $\tilde{r}$ the one that minimizes the generalized distance [20]

$$d_{\text{GD}}(r, \tilde{r}) = \sum_{i: r_i = \tilde{r}_i} (1 - \alpha_i) + \sum_{i: r_i \neq \tilde{r}_i} (1 + \alpha_i),$$

where $\alpha_i \equiv \frac{|L_i|}{\max_{1 \leq j \leq n} |L_j|}$. Note that if all input LLRs $L_j$ have the same magnitude, we have $\alpha_i = 1$ for all $i = 1, \ldots, n$ and (3) reverts to $2d_H(r, \tilde{r})$.

III. ITERATIVE DECODING OF PRODUCT CODES

PCs can be decoded by applying BDD of the row and column codes in an iterative manner. This algorithm is referred to as iBDD. In the following, two other algorithms that can improve the performance of iBDD are described.
A. Anchor Decoding

When a miscorrection occurs during iBDD, it is possible that two component codes disagree on the value of a particular bit, leading to a conflict. Conflicts are typically ignored in the sense that row and column codes are decoded sequentially and previous decoding decisions are simply overridden. The main idea in AD is to introduce status information for each component code and designate certain “reliable” component codes as anchors. Then, no further additional corrections from other component codes are allowed if this would lead to a conflict and overturn the decision of an anchor. Since some anchors may actually be miscorrected, AD also allows for the backtracking of the decoding decisions of anchors. This happens whenever too many other component codes are in conflict with a particular anchor. Pseudocode for AD can be found in [17, Alg. 2].

B. Iterative Bounded Distance Decoding With Scaled Reliability

Both iBDD and AD do not take potentially available channel reliability information into account. In [18], we proposed a modification of iBDD where channel reliabilities are exploited, while only binary messages between component decoders are exchanged. This algorithm is referred to as iBDD with scaled reliability (iBDD-SR). In particular, assume that the $i$-th row code has been decoded via BDD. In order to combine the BDD output with the channel LLRs, the decoded bits are mapped according to $0 \rightarrow +1$ and $1 \rightarrow -1$ if BDD is successful and mapped to 0 if a decoding failure occurs. Let $\tilde{\mu}_{r,i}^{\ell} \in \{\pm 1, 0\}$ be the result of this mapping for the decoded bit corresponding to code bit $c_{i,j}$ in iteration $\ell$. Then, we compute

$$\psi_{i,j}^{\ell} = B(w_\ell \cdot \tilde{\mu}_{i,j}^{\ell} + L_{i,j}),$$

where $w_\ell > 0$ is a scaling parameter and $\psi_{i,j}^{\ell}$ can be interpreted as the message passed from the $i$-th row code to the $j$-th column code. In particular, after applying this procedure to all row codes, the matrix $\Psi^{\ell} = [\psi_{i,j}^{\ell}]$ is used as the input for the column codes, where BDD based on $\Psi^{\ell}$ is performed. The binary output messages for the row codes are then formed in a similar fashion as for the column codes. Intuitively, the mapping (4) helps to alleviate the effect of miscorrections by allowing the outcome of BDD at certain bit positions to be overturned if the corresponding channel LLR is very reliable (i.e., $|L_{i,j}|$ is large).

IV. ITERATIVE GENERALIZED MINIMUM DISTANCE DECODING WITH SCALED RELIABILITY

In this section, we propose a novel iterative decoding algorithm for PCs based on GMD decoding of the component codes and the exchange of soft information between component codes. We refer to this algorithm as iGMDD-SR.

iGMDD-SR works as follows. Without loss of generality, assume that the decoding starts with the row codes and let us consider the decoding of the $i$-th row code at iteration $\ell$. Let $\tilde{\mu}_{i,j}^{\ell}$ be the vector of soft information corresponding to $C_{i,j}$ at the input of the $i$-th row decoder at iteration $\ell$, resulting from the decoding of the $c_{i,j}$ column codes at decoding iteration $\ell - 1$, where, initially, $\tilde{\mu}_{i,j}^{0} = L_{i,j}$. Also, let $R_{i,j}^{\ell} = B(\tilde{\mu}_{i,j}^{\ell})$ be the corresponding hard-decoded vector. Then, GMD decoding of the $i$-th row code is performed as explained in Section II-B based on $R_{i,j}^{\ell}$ and the reliabilities $|\tilde{\mu}_{i,j}^{\ell}|$. Note that GMD decoding does not provide reliability information about the decoded bits, i.e., it is “soft-input, hard-output”. In order to provide reliability information to the column decoders, we resort to a heuristic approach that is similar to the approach used for iBDD-SR. In particular, the output bits of GMD decoding are mapped according to $0 \rightarrow +1$ and $1 \rightarrow -1$ if GMD decoding is successful and mapped to 0 if GMD decoding fails. Let $\tilde{\mu}_{i,j}^{\ell} \in \{\pm 1, 0\}$ be the result of this mapping for the decoded bit corresponding to code bit $c_{i,j}$. The reliability information is then formed according to

$$\mu_{i,j}^{\ell} = w_\ell \cdot \tilde{\mu}_{i,j}^{\ell} + L_{i,j},$$

where $w_\ell > 0$ is a scaling parameter and $\mu_{i,j}^{\ell} = (\mu_{i,j}^{\ell}, \ldots, \mu_{i,1}^{\ell})$ is the entire soft-output vector of the $i$-th row decoder.

Visualizing the decoding over the Tanner graph of the code, $\mu_{i,j}^{\ell}$ corresponds to the message from row $C_{i,n}$ to column $C_{j,n}$. Now assume that all row codes have been decoded. The vector of soft information corresponding to $C_{i,j}$ at the input of the $j$-th column decoder is then defined as $\mu_{j}^{\ell} = (\mu_{j,1}^{\ell}, \ldots, \mu_{j,n}^{\ell})$. GMD decoding is performed based on $R_{i,j}^{\ell} = B(\mu_{j}^{\ell})$ and $|\mu_{j}^{\ell}|$. The soft output of the $j$-th column decoder is formed similar to (5) and the resulting soft output vector is denoted by $\mu_{j}^{\ell+1} = (\mu_{j,1}^{\ell+1}, \ldots, \mu_{j,n}^{\ell+1})$, where $\mu_{j}^{\ell+1}$ corresponds to the message from column $C_{i,n}$ to row $C_{j,n}$. After decoding all column component codes, we set $\mu_{i,j}^{\ell+1} = (\mu_{i,1}^{\ell+1}, \ldots, \mu_{i,n}^{\ell+1})$ and the iterative process continues until a maximum number of iterations is reached. The information flow from the row to column codes in iGMDD-SR is schematically illustrated in Fig. 2.

V. DECODING COMPLEXITY DISCUSSION

A thorough complexity analysis of the different decoding algorithms presented in Sections II-A, III-B, and IV is a formidable task that should include, besides the pure algorithmic aspects, also the implications in terms of internal data flow. A complete analysis is therefore out of the scope of this paper. We however provide a high-level discussion of
The use of BDD to decode the component codes represents the simplest approach among those considered. From this viewpoint, iBDD, AD, and iBDD-SR are characterized by a similar complexity. For iBDD-SR, the combination of the BDD output and the channel LLRs in (4) yields a small complexity increase with respect to iBDD and AD. With respect to BDD of the component codes, GMD decoding entails more substantial changes in the decoder. In this case, the component decoder has to be provided with soft decisions by the previous decoding step. Finally, t error-erasure decoding attempts and one BDD attempt are required. Each error-erasure decoding attempt has a cost close to a run of BDD. Each decoding attempt may result in a candidate codeword that is used to form a list of size up to $t+1$. The minimization of the distance in (3) has a negligible cost with respect to the $t+1$ decoding attempts.

The decoding complexity of TPD exceeds the complexity of AD, iBDD-SR, and iGMDD-SR. In particular, the Chase–Pyndiah algorithm requires the construction of a list of binary test sequences for each component decoding, where the list size depends on a design parameter. Typically, the list size is set to at least 16 [13], and BDD is applied to each test sequence. Thus, for components codes where $t$ is small (e.g., 2, 3, or 4), as the ones considered in this paper and of practical use for high-throughput fiber-optic communications, the list size and corresponding cost per component decoding in GMD decoding is only a fraction of that of TPD. Moreover, iGMDD-SR also relaxes the computational requirements when computing the extrinsic soft-output information for each code bit compared to TPD by using the heuristic update equation in (5).

VI. SIMULATION RESULTS

In this section, we compare the product decoding algorithms in terms of their performance. For the simulations, we consider double-error-correcting extended BCH (eBCH) codes with parameters (256, 239, 6) as component codes. The resulting PC has rate $R = 239^2/256^2 \approx 0.8622$ corresponding to an FEC overhead of $1/R - 1 \approx 15\%$. For all algorithms, a maximum of $t_{\text{max}} = 10$ decoding iterations is performed.

Both iBDD-SR and iGMDD-SR require a proper choice for the scaling factors $w_k$ in each iteration. We jointly optimize all scaling factors $w = (w_1, \ldots, w_{t_{\text{max}}})$ by using Monte–Carlo estimates of the bit error rate (BER) for a fixed $E_b/N_0$ as the optimization criterion. Intuitively, one would expect that the decisions of the component decoders become more reliable with iterations, whereas the channel observations become less informative. Therefore, in order to reduce the optimization search space, we only consider vectors $w$ with monotonically increasing entries. For iBDD-SR, we found that the optimized vector $w$ is relatively insensitive to the targeted $E_b/N_0$. On the other hand, iGMDD-SR is more sensitive to a mismatch between the optimized and actual $E_b/N_0$ and the optimization is thus performed for each value of $E_b/N_0$ separately.

In Fig. 3, the performance of iBDD, AD, iGMDD-SR, and iBDD-SR is shown. We also plot the performance of TPD via off-the-shelf Matlab toolbox functions and compare to a commercially available 100 Gb/s SD-FEC solution implementing TPD for the same overhead [15]. The data points are directly extracted from [15], but we remark that the component code details are not disclosed in [15]. Thus, a different PC may be used. Moreover, pre- and post-processing steps are employed, which may also explain the performance difference.

AD and iBDD-SR outperform the conventional iBDD by 0.18 dB and 0.25 dB at a bit error rate (BER) of $10^{-5}$, respectively. As a reference, we show the performance of idealized iBDD, where a genie prevents all miscorrections. The asymptotic performance of idealized iBDD can be analytically predicted by using density evolution [22], [23], which is shown by the dotted line. It can be seen that both AD and iBDD-SR are effective algorithms to combat miscorrections. The performance degradation of iBDD-SR compared to ideal iBDD is very small ($< 0.01$ dB), implying that by properly tuning the scaling parameters $w$, iBDD-SR can alleviate the effect of miscorrections to a large extent.

One can also see that iGMDD-SR outperforms iBDD, AD, and iBDD-SR. In particular, the performance gain of iGMDD-SR over iBDD is 0.60 dB at a BER of $10^{-5}$. The additional performance gain is expected, since GMD decoding can decode beyond half the minimum distance by introducing erasures and performing multiple error-erasure component decoding attempts. Furthermore, iGMDD-SR performs 0.52 dB away from TPD, i.e., it closes over 50% of the performance gap between iBDD and TPD.
The net coding gain improvements of all considered decoding algorithms over iBDD are summarized in Table I. We also indicate the gap to capacity for all schemes. Note that the performance of iBDD and AD should be compared to the HD capacity, whereas the performance of iBDD-SR, iGMDD-SR, and TPD should be compared to the SD capacity since channel LLRs are exploited during decoding. Overall, one can see a clear trade-off between performance and complexity for the different algorithms, e.g., using iGMDD-SR, with higher complexity than iBDD, yet less complexity than TPD, the gap between iBDD and TPD is approximately halved.

VII. CONCLUSION

We studied several low-complexity iterative decoding algorithms for PCs that outperform the conventional iBDD. In particular, we reviewed two previously proposed algorithms, AD and iBDD-SR, and we proposed a novel algorithm called iterative GMD decoding with scaled reliability (iGMDD-SR). For the considered scenario based on double-error-correcting eBCH component codes, AD and iBDD-SR outperform iBDD by 0.18 dB and 0.25 dB, respectively, with only a small increase in complexity. The complexity increase for iGMDD-SR is larger, but the algorithm achieves a more significant performance gain of 0.60 dB over iBDD. This closes over 50% of the performance gap to TPD, at a significantly lower complexity.

REFERENCES

[1] A. Leven and L. Schmalen, “Status and recent advances on forward error correction technologies for lightweight systems,” IEEE/OSA J. Lightw. Technol., vol. 32, no. 16, pp. 2753–2755, Aug. 2014.
[2] L. Schmalen, V. Aref, J. Cho, D. Siukat, D. Röser, and A. Leven, “Spatially coupled soft-decision error correction for future lightweight systems,” IEEE/OSA J. Lightw. Technol., vol. 33, no. 5, pp. 1109–1116, Mar. 2015.
[3] C. Häger, A. Graell i Amat, F. R. Kschischang, “Terminated and tailbiting spatially coupled codes with optimized bit mappings for spectrally efficient fiber-optical systems,” IEEE/OSA J. Lightw. Technol., vol. 33, no. 7, pp. 1275–1285, Apr. 2015.
[4] L. M. Zhang and F. R. Kschischang, “Low-complexity soft-decision concatenated LDGM-staircase FEC for high-bit-rate fiber-optic communication,” IEEE/OSA J. Lightw. Technol., vol. 35, no. 18, pp. 3991–3999, Sep. 2017.
[5] M. Barakat and F. R. Kschischang, “Low-complexity concatenated LDPC-staircase codes,” IEEE/OSA J. Lightw. Technol., vol. 36, no. 12, pp. 2443–2449, Jun. 2018.
[6] B. Smith and F. R. Kschischang, “A Pragmatic Coded Modulation Scheme for High-Spectral-Efficiency Fiber-Optic Communications,” J. Lightw. Technol., vol. 30, no. 13, pp. 2047–2053, Jul. 2012.
[7] C. Häger, A. Graell i Amat, H. D. Pfister, and F. Brännström, “Density Evolution for Deterministic Generalized Product Codes with Higher-Order Modulation,” in Proc. Int. Symp. Turbo Codes and Iterative Information Processing (ISTC), Brest, France, Sep. 2016, pp. 236–240.
[8] A. Sheikh, A. Graell i Amat, G. Liva, and F. Steiner, “Probabilistic Amplitude Shaping with Hard Decision Decoding and Staircase Codes,” IEEE/OSA J. Lightw. Technol., vol. 36, no. 9, pp. 1689–1697, May 2018.
[9] B. P. Smith, A. Farhood, A. Hunt, F. R. Kschischang, and J. Lodge, “Staircase codes: FEC for 100 Gb/s OTN,” IEEE/OSA J. Lightw. Technol., vol. 30, no. 1, pp. 110–117, Jan. 2012.
[10] A. J. Felstöm, D. Truhaček, M. Lentmaier, and K. S. Zigangirov, “Braided Block Codes,” IEEE Trans. Inf. Theory, vol. 55, no. 6, pp. 2640–2658, Jul. 2009.
[11] Y. Y. Jian, H. D. Pfister, K. R. Narayanan, R. Rao, and R. Mazahreh, “Iterative hard-decision decoding of braided BCH codes for high-speed optical communication,” in Proc. IEEE Global Telecommun. Conf. (GLOBECOM), Dec. 2013, pp. 2376–2381.
[12] P. Elias, “Error-free coding.” Trans. IEEE Professional Group on Inf. Theory, vol. 4, no. 4, pp. 29–37, Sep. 1954.
[13] R. M. Pyndiah, “Near-optimum decoding of product codes: block turbo codes,” IEEE Trans. Commun., vol. 46, no. 8, pp. 1003–1010, Aug. 1998.
[14] C. Condo, P. Giard, F. Leduc-Primeau, G. Sarkis, and W. J. Gross, “A 9.52 dB NCG FEC scheme and 162 b/Cycle low-complexity product decoder architecture,” IEEE Trans. Circuits and Systems I, vol. 65, no. 4, pp. 1420–1431, Apr. 2018.
[15] Viasat Inc., “ECC66100 series SD-FEC encoder/decoder cores,” 2017.
[16] C. Fougstedt and P. Larsson-edefors, “Energy-Efficient High-Throughput Decoder Architecture,” in Proc. Optical Fiber Communication Conf. (OFC), San Diego, CA, Mar. 2018, pp. 1–3.
[17] C. Häger and H. D. Pfister, “Approaching Miscorrection-free Performance of Product Codes with Anchor Decoding,” IEEE Trans. Commun. (to appear), 2018.