Wireless Powering Efficiency Assessment for Deep-Body Implantable Devices

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Abstract—Several frequency-dependent mechanisms restrict the maximum achievable efficiency for wireless powering implantable bioelectric devices. Similarly, many mathematical formulations have been proposed to evaluate the effect of these mechanisms as well as predict this maximum efficiency and the corresponding optimum frequency. However, most of these methods consider a simplified model, and they cannot tackle some realistic aspects of implantable wireless power transfer. Therefore, this paper proposed a novel approach that can analyze the efficiency in anatomical models and provide insightful information on achieving this optimum operation. First, this approach is validated with a theoretical spherical wave expansion analysis, and the results for a simplified spherical model and a bidimensional human pectoral model are compared. Results have shown that even though a magnetic receiver outperforms an electric one for near-field operation and both sources could be equally employed in far-field range, it is in mid-field that the maximum efficiency is achieved, with an optimum frequency between 1–5 GHz, depending on the implantation depth. In addition, the receiver orientation is another factor that affects the efficiency, with a maximum difference between the best and worst-case scenarios around five times for an electric source and over 13 times for the magnetic one. Finally, this approach is used to analyze the case of a wirelessly powered deep-implanted pacemaker by an on-body transmitter and to establish the parameters that lead to the maximum achievable efficiency.

Index Terms—Biomedical electronics, implants, pacemakers, radiation efficiency, wireless power transfer.

I. INTRODUCTION

WIRELESS Power Transfer (WPT) has been the subject of many works and publications mainly due to its technological and commercial appeal. It was founded in the works of Nikola Tesla, who in the first place proposed the use of electromagnetic waves to wirelessly power electric devices. Even though the theoretical aspects have been studied throughout the years and are well consolidated, the physical realization and the proposition of different techniques for its application have gained a stronger impulse in the last 20 years [1]. Overall, one way to classify the different WPT techniques that use electromagnetic waves as the energy carriers is by the radiation region that comprises the distance between the transmitter and receiver. For instance, the near-field techniques are based on the near-field coupling between antennas that can be either inductive or capacitive [2]. Consequently, due to the short distance between antennas, these techniques can achieve high efficiency, and they are able to deliver high power levels [3]. This efficiency can be even further increased by electromagnetic resonance [4]. On the other side, the radiative or far-field techniques can cover a wide distance range with the drawback of lower efficiency. Therefore, they usually employ highly directive antennas to reduce the power dispersed in free-space and thus, increase the received power [5]. A new mid-field wireless power transfer technique has been proposed to achieve higher efficiency than the far-field techniques and larger distance ranges than their near-field counterparts. In mid-field WPT, the distance between transmitter and receiver is in the order of a wavelength, and, in this case, the electromagnetic fields are composed of reactive and propagating components [6], [7].

In the context of biomedical engineering, the application of WPT for implantable bioelectronic and biosensor devices is envisaged to monitor physiological processes [8], drug delivery [9], and organ stimulation through electric signals [10], to name a few. Therefore, the different WPT techniques have already been applied for wireless powering bioelectronic implants. For instance, near-field WPT is employed for subcutaneous pacemakers [11], [12], neural and spinal cord stimulators [13], cochlear [14], and ocular implants [15] among other. All these applications share the same characteristic of having a small implantation depth. Conversely, far-field techniques are used for ultra-low-power implants usually applied for biotelemetry [8]. However, for powering deep-implanted devices, the mid-field WPT is mostly used. For example, it has been applied for cardiac implants and pacemakers [16]–[18], gastrointestinal endoscopy capsules [19], [20], and neural implants [21].

Several physical, technical, and legal aspects impose limitations to the in-body WPT application. First, the body tissues are composed of dynamic, highly heterogeneous, dispersive, and lossy media that deteriorate the efficiency of WPT techniques which in other applications presents a reasonable efficiency. The two prominent factors that reduce WPT efficiency are the electromagnetic wave attenuation in these lossy tissues, which is proportional to the operating frequency, and the reflection in the interface between different media [22]. Moreover, the miniaturized implantable receivers are usually both physically and electrically small, further reducing
the maximum achievable efficiencies \([23]\), not to mention other sources of losses such as impedance mismatching, misalignments, and internal resonances in the body organs. Apart from that, another major concern is the exposure to the electromagnetic fields once some WPT techniques can lead to hazardous exposure levels \([24]\). Therefore, the WPT system parameters — such as operation frequency, nature of the source, and implantation depth — must be judiciously chosen in order to achieve the highest efficiency possible, taking into account the exposure level regulations.

Several models have been proposed to mathematically assess the maximum radiation efficiency and optimal frequency for implantable bioelectronic devices. The planar stratified heterogeneous model \([25], [26]\) is a simple approach that allows an analytical formulation that includes the wave reflection between different layers. In this model, the equivalence principle replaces a volumetric surface current distribution for an in-plane electric current density source that produces the same electromagnetic fields. Although this model is mathematically more straightforward and provides a physical inside of the problem under analysis, it considers the human body as planar and infinite media. On the other hand, the spherical wave expansion \([27]–[29]\) is a semi-analytical approach that represents the human body as a spherical model composed of a homogenous or concentric multilayered medium. In this case, the source is represented by an electric or magnetic dipole encapsulated by a small sphere positioned anywhere inside the spherical phantom. Then, the electric and magnetic fields are decomposed in vector spherical harmonics, and, from orthogonality relationships, the problem is mathematically solved by a linear system. This approach is computationally simpler than a full-wave analysis and can lead to insightful results once the level of achievable power density just outside the body is mainly influenced by the source position than the shape of the phantom itself. However, this approach is difficult to implement for more complex sources and realistic body models. For this intend, a full-wave computation needs to be carried out to solve the inhomogeneous wave equation numerically given an arbitrary finite-sized source \([23]\).

This work aims to investigate the electromagnetic energy exchange between an optimal on-body transmitter and an implantable receiver, as well as to analyze the influence of the system’s parameters on the wireless power transfer efficiency. For this intend, a general 2D-axisymmetric full-wave approach is developed, providing the best-case scenario for the energy transfer efficiency as a function of the frequency, the implantation depth, and the nature of the receiver, i.e., electric or magnetic. The basis for this problem formulation and some results for a simplified spherical phantom model have been presented \([30]\). However, the proposed approach is further extended and validated with a theoretical model based on spherical wave expansion in this paper. Then, both methods are used to evaluate the frequency-dependent radiation efficiency for several implantation depths considering electric and magnetic receivers, and these results surpass the efficiency levels previously presented in the literature with other approaches.

Previous studies on modeling electromagnetic wave propagation in the human body mainly focused on wireless communications with implantable antennas \([28], [31]\) medical treatments based on electromagnetic waves such as hyperthermia \([32]–[35]\), or dosimetry \([36]\). However, the investigation of wave propagation for WPT applications \([16], [23]\) involves a specific focus on the electromagnetic interaction between an on-body transmitter and an in-body receiver. Therefore, the optimal operating conditions identified for in-body biotelemetry and hyperthermia applications might differ from the WPT ones. Specifically, for the in-body biotelemetry, the goal is essentially to maximize the omnidirectional radiation performance through the high-contrast tissue–air interface \([22]\). For hyperthermia, the main objective is to control the local and non-linear \([\text{i.e., } \varepsilon(E)]\) absorption of energy close to the source \([33]\). As a result, most deep-body implantable devices operate in the MedRadio band \((401–457 \text{ MHz})\) \([37]\); the optimal band for hyperthermia is between 130 MHz and 500 MHz \([38]\), whereas for WPT, the maximum efficiency is achieved around 1–3 GHz \([25], [26], [30], [39]\). This work studies the electromagnetic exchange in an in-/on-body WPT system, derives, and demonstrates the optimal operating conditions in terms of efficiency and exposure as a function of implantation depth and nature of the power source antenna.

Moreover, this study applies for the first time the 2D-axisymmetric full-wave formulation to assess the wireless power transfer efficiency in an anatomical scenario considering a deep-implanted mm-sized pacemaker in a transverse cut model for the human pectoral. In this way, it is possible to analyze the real-life application of WPT for powering a cardiac stimulator such as presented in \([16]\). In addition, different configurations for electric and magnetic on-body sources are investigated, and the results for the anatomical model are compared with the simplified spherical phantom. Finally, the origin for the losses is discussed from these results, and ways to mitigate them and achieve maximum efficiency are investigated from parametric analysis of on-body transmitter that wirelessly powers the implanted pacemaker.

II. Efficiency Assessment Using The Simplified Spherical Model

The problem under analysis consists of a wireless power transfer system composed of an implantable bioelectronic device that acts as a receiver and a transmitter radiating structure conformal to the body. In order to determine the achievable wireless power transfer efficiency, the human body is modeled as a dispersive homogeneous spherical phantom of radius \(R_p\) with complex permittivity \(\varepsilon_r(f)\) equivalent to the human muscle tissue \([40]\), as is shown in Fig. [I]. Inside this phantom, the implantable device is represented as a lossless \(\varepsilon_r(f)\) capsule-shaped, perfectly matched to the wave impedance in the surrounding tissue, length \(L_t\), and radius \(R_c\). This spherical model allows comparing the results obtained with the proposed approach to semi-analytical solutions based on spherical wave expansion. In addition, this simplified model disregards the shape complexities and heterogeneities leading to more general results that are better suitable for an initial analysis of implantable wireless power transfer systems.
To eliminate losses due to reflection on the interface between the body and the external medium and thereby ensure the maximum WPT efficiency, the permittivity of the region around the phantom is considered as the real part of $\varepsilon_r(f)$, i.e., the external medium is lossless $\varepsilon_r(f)$ and matched to the wave impedance in the muscle. In this way, the on-body transmitter is well matched to the tissue, which can be physically realized using a high dielectric constant layer. In addition, this model disregards any impedance mismatches in the antennas and any system-level losses in electronic circuitry.

To mathematically formulate the problem under analysis, an equivalent problem can be proposed based on reciprocity [41]. For this intent, the radiation source is modeled as the electric current density distribution $J_s$ inside the phantom, as indicated in Fig. 1b. The reciprocity can be applied in this case once the medium is linear and there is no polarization mismatch. Consequently, the radiated fields induce a power flow in the lossy phantom and, from energy conservation, the transmitted power $P_t$ is given by:

$$P_t = P_r + P_d + i2\omega(W_m - W_e), \quad (1)$$

where $P_r$ and $P_d$ are respectively the received and dissipated powers, whereas $W_m$ and $W_e$ are the time-average magnetic and electric energies, respectively.

From the time-harmonic electric $E$ and magnetic $H$ fields, as well as the source electric $J_s$ and magnetic $M_s$ current densities, each one of the total power components can be calculated as follow:

$$P_t = \oint_{\Omega_s} \left( \frac{1}{2} E \times H^\ast \right) \cdot ds, \quad (2a)$$

$$P_r = \oint_{\Omega_p} \left( \frac{1}{2} E \times H^\ast \right) \cdot ds, \quad (2b)$$

$$P_d = \frac{1}{2} \int_{\Omega_p} \sigma |E|^2 \, dv, \quad (2c)$$

where $\sigma$ is the phantom’s electric conductivity conductivity which is related to the imaginary part of the phantom’s complex permittivity $\Im[\varepsilon_r(f)]$ through $\sigma(f) = 2\pi \Im[\varepsilon_r(f)]$. The integration domains $\Omega_s$ and $\Omega_p$ indicate that the integral is performed on the surface of the source and the phantom, respectively. Besides, the integrals (2a-2c) can be considerably simplified due to the problem’s axial symmetry. Finally, the wireless power transfer efficiency $\eta$ is defined as:

$$\eta \equiv \frac{\Re(P_r)}{\Re(P_t)} = 1 - \frac{\Re(P_d)}{\Re(P_t)}, \quad (3)$$

with $\Re$ being the real part of the complex variable under brackets.

Hereafter, the implantable bioelectric device is referred to as the receiver antenna, whereas the transmitter antenna is the radiating on-body structure.
A. Full-wave 2D-Axisymmetric Analysis

In order to numerically evaluate the wireless power transfer efficiency using the proposed approach, this model was implemented using the full-wave 2D-axisymmetric formulation available in COMSOL Multiphysics (it is assumed that there is no variation of electromagnetic fields in the \( \varphi \) direction). Electric and magnetic sources, with size \( L = 1 \) cm and \( R_c = L/3 \) are considered in this computation. Each source is represented by the electric \( \mathbf{J}_s^E(r, \varphi, z) \) and magnetic \( \mathbf{J}_s^H(r, \varphi, z) \) surface current densities given by (23):

\[
\mathbf{J}_s^E = \begin{bmatrix} 0, 0, \cos \left( \frac{\pi z}{L} \right) \end{bmatrix}, \quad (4a)
\]
\[
\mathbf{J}_s^H = [0, 1, 0]. \quad (4b)
\]

Then, the wireless power transfer efficiency in (3) can be calculated from the evaluated integrals (2a),(2c).

B. Spherical Wave Expansion Analysis

The results from a semi-analytical approach based on spherical-wave modal expansion are used as a reference to validate the proposed model. In this model depicted in Fig. 1, the electromagnetic fields \( \mathbf{E} \) and \( \mathbf{H} \) in a spherical structure free of charges can be expressed using spherical harmonics \( \mathbf{M} \) and \( \mathbf{N} \) [41]:

\[
\begin{align*}
\mathbf{E} \\
\mathbf{H}
\end{align*} = \sum_{n,m} a_{mn} \begin{bmatrix} \mathbf{M}_{mn} \\
\mathbf{N}_{mn} \end{bmatrix} + b_{mn} \begin{bmatrix} \mathbf{N}_{mn} \\
\mathbf{M}_{mn} \end{bmatrix}, \quad (5)
\]

with

\[
\mathbf{M}_{mn} = \nabla \times \mathbf{r} \psi_{mn}, \quad (6a)
\]
\[
\mathbf{N}_{mn} = \frac{1}{k} \nabla \times \nabla \times \mathbf{r} \psi_{mn}, \quad (6b)
\]

where \( k \) denotes the wave number of the considered media, \( \mathbf{r} \) is the unit position vector in the \( r \)-direction, and \( \psi_{mn} \) is the solution to the Helmholtz differential equation:

\[
\psi_{mn} = \frac{1}{kr} Z_n(kr) P^m_n(\cos \theta) e^{im\varphi}. \quad (7)
\]

The Schelkunoff type spherical Bessel or Hankel functions are indicated by \( Z_n \), whereas \( P^m_n \) are the associated Legendre functions of the first kind [42]. From the orthogonality relationships for spherical harmonics, the equation (5) becomes a linear system whose solution provides the modal representation for the electromagnetic fields. More details about this implementation can be found in [28].

The integrals (2a),(2c) can be evaluated from the spherical model coefficients and vectors and, thus, the efficiency can be obtained through (3). It is important to notice that this theoretical approach can also be applied to off-centered sources [27],[28].

C. Results and Discussion

The wireless power transfer efficiency for the electric \( \eta_E \) and magnetic \( \eta_H \) sources were evaluated from the electromagnetic fields calculated through the 2D-Axisymmetric model (2DA) and the Spherical Wave Expansion (SWE) model. In Fig. 2 the efficiency for both sources is shown as a function of the frequency for different phantom radius, which is asymptotically equivalent to the variation in the implantation depth. Besides, the chosen range comprises most of the applications for wireless powered implants, from subcutaneous to deeply implanted devices.

First of all, the results obtained from the two approaches previously described are compared. As it can be seen, the efficiency evaluated with the 2D-Axisymmetric model agrees with the one calculated with Spherical Wave Expansion, especially at the vicinity of the optimum frequency in which the error between them is 0.64% for the electric receiver and 2.07% for the magnetic one. However, for lower frequencies, an offset between them is noticeable mainly due to the difference in the source formulation.

![Fig. 2. Wireless power transfer efficiency for an (a) electric \( \eta_E \) and (b) magnetic \( \eta_H \) receiver as a function of the frequency and the phantom radius \( R_p \) (asymptotically equivalent to the implantation depth) evaluated through the 2D-Axisymmetric (2DA) and the Spherical Wave Expansion (SWE) models.](image-url)
plantation depths. It becomes clear from Table I once the optimum frequency for the magnetic receiver is below the far-field region, roughly starting at 1 GHz. In addition, at the near-field region, $\eta_E$ sharply increases until reaching its maximum, whereas $\eta_H$ initially increases then reaches a plateau at the maximum efficiency. Conversely, both receivers present similar decaying behavior in the far-field region, and $\eta_H$ asymptotically approaches $\eta_H$ at frequencies above the optimum one for the electric receiver.

As the reflection losses can be disregarded, this overall behavior for both receivers can be explained by the fact that in low frequencies, the near-field losses are higher, whereas, in the far-field region, the attenuation losses become more significant [27]. Thus, the optimum frequency corresponds to the trade-off point between both loss mechanisms. Moreover, once the near-field losses affect more electric than magnetic sources, the efficiency at low frequencies is significantly lower for this receiver.

![Table I](image)

| $R_p$ (mm) | Electric Receiver | Magnetic Receiver |
|------------|-------------------|-------------------|
| 20         | 35.44% at 1.26 GHz | 44.92% at 794.3 MHz |
| 37         | 13.43% at 1.26 GHz | 19.01% at 398.1 MHz |
| 50         | 6.83% at 1 GHz     | 10.44% at 631 MHz  |
| 100        | 0.49% at 1 GHz     | 2.036% at 100 MHz  |

The analysis carried out in this paper considers fixed dimensions for the receiver. However, a further study on the peak efficiency and optimum frequency dependence on the receiver dimensions is presented in [23]. It has shown that the receiver length $L$ is the parameter that most impacts the efficiency; for instance, the larger the electric source, the higher the efficiency will be. On the other hand, for a magnetic source, the peak efficiency is reached within the range $1.5Rc < L < 3Rc$. In addition, the fundamental limit on the electrically small antennas efficiency states that a reduction in the receiver size will also lead to a reduction in its radiation efficiency. Therefore, the receiver size considered in the previous analysis not only is in the range that leads to maximum efficiency but also corresponds to the size of practical implementation of implantable and ingestible antennas [37].

### III. Efficiency Assessment Using the Anatomical Pectoral Model

A 2D heterogeneous model of the human pectoral region in Fig. 1, with nine dispersive media with complex permittivity equivalent to those in the different human tissues [40], was implemented in COMSOL Multiphysics in order to analyze the wireless powering efficiency in a more realistic scenario. Based on the wirelessly powered pacemaker proposed in [16], the receiver is represented by a circular region with a radius of 1 mm inside the heart with implantation depth $d$ equal to 37 mm.

Similarly as described for the spherical model in Section II, the electric permittivity of the region external to the body is the same as a lossless skin $\varepsilon_{skin}(f)$, whereas the also lossless medium inside the pacemaker $\varepsilon_{muscle}(f)$ is perfectly matched to the wave impedance of the myocardium. In this way, the reflection losses can be disregarded.

For the analysis of this problem as a 2D model, it is assumed that the implantable receiver and the on-body transmitter are perfectly aligned, and therefore the $z$-axis invariance is valid, i.e., $\mathbf{E}(x, y, z) = \mathbf{E}(x, y)e^{ik_zz}$, where $k_z$ is the out-of-plane propagation constant. Moreover, due to the high tissue dispersivity, the radiated power is attenuated at short distances from the transmitter. Therefore, the computational cost can be reduced by analyzing only the cross-section of the body region in which the receiver is implanted.

The same approach described in Section II was applied to the 2D pectoral model to calculate the maximum wireless power transfer efficiency in a realistic scenario and compare these results with those obtained with the simplified spherical model. The reciprocity theorem is again evoked for calculation purposes, and the radiation source is considered inside the heart. This premise is still valid once the different media are linear and there is no polarization mismatch. Consequently, the obtained efficiency calculated with (3) is valid for the original problem of powering the implantable device.

However, differently from the 2D-axisymmetrical case, different receiver configurations and orientations can be used in the realistic planar model, as shown in Fig. 3.

Fig. 3. Different receiver configurations are used for the realistic model analysis. An electric receiver can be defined through (a) a surface electric current distribution $J^E_s$, (b) an electric point dipole $\mathbf{n}^E_x$, and (c) an out-of-plane magnetic current $I_M^H$. Alternatively, a magnetic receiver can be modeled as (d) a surface magnetic current distribution $J^H_s$, (e) a magnetic point dipole $\mathbf{n}^H_x$, and (f) an out-of-plane line current $I_E$. The contour lines depict the electric $\mathbf{E}$ and magnetic $\mathbf{H}$ field distribution in arbitrary units.

The first possibility is to assign a Surface Current Distribution (SCD) over the line of length $L$ (in the 2D simulation) for the electric $J^E_s(x, y, z)$ and magnetic $J^H_s(x, y, z)$ receivers according to:

$$
J^E_s = \begin{cases} 
\cos \left( \frac{\pi x}{L} \right) A/m \hat{y}, & \text{if vertically oriented} \\
\cos \left( \frac{\pi y}{L} \right) A/m \hat{x}, & \text{if horizontally oriented}
\end{cases}
$$ (8a)
\[ \mathbf{J}_s^H = \begin{cases} 1 \text{ V/m} \hat{\mathbf{y}}, & \text{if vertically oriented} \\ 1 \text{ V/m} \hat{\mathbf{x}}, & \text{if horizontally oriented.} \end{cases} \] (8b)

Henceforward, vertically oriented means that the receiver is oriented in the \( y \)-axis direction (\( \hat{\mathbf{y}} \)) whereas horizontally oriented in the \( x \)-axis direction (\( \hat{\mathbf{x}} \)), according to the coordinate system depicted in Fig. 3.

Subsequently, the next alternative is to define the receiver as an Electric Point Dipole (EPD) or Magnetic Point Dipole (MPD). In each one, the electric \( \mathbf{n}_p^E \) or magnetic \( \mathbf{n}_p^H \) dipole moment vector is assigned as follows:

\[ \mathbf{n}_p^E = \begin{cases} 1 \text{ A-m} \hat{\mathbf{y}}, & \text{if vertically oriented} \\ 1 \text{ A-m} \hat{\mathbf{x}}, & \text{if horizontally oriented}, \end{cases} \] (9a)

\[ \mathbf{n}_p^H = \begin{cases} 1 \text{ A-m}^2 \hat{\mathbf{y}}, & \text{if vertically oriented} \\ 1 \text{ A-m}^2 \hat{\mathbf{x}}, & \text{if horizontally oriented}. \end{cases} \] (9b)

Finally, it is also possible to define an out-of-plane Magnetic Current (MC) for modeling the electric receiver or an out-of-plane Line Current (LC) for the magnetic one. Respectively for each case, the electric or magnetic fields are orthogonal to the current distribution direction and the position vector. Therefore, the out-of-plane magnetic \( I_M = 1 \text{ V} \) and electric \( I_E = 1 \text{ A} \) currents must be assigned following the direction and orientation shown in Fig. 3c and Fig. 3f, respectively.

By taking into account the three source types and the vertical and horizontal orientations, it leads to six possible configurations for each electric and magnetic receiver. Finally, the wireless power transfer efficiency was evaluated for all the described scenarios, and the results are presented in Fig. 4. It is possible to see that the efficiencies evaluated with different sources agree between them, which demonstrates the flexibility of the proposed model for dealing with different source configurations.

The source orientation is the factor that mainly affects the radiation efficiency. In the best-case scenario, the sources are horizontally-oriented, whereas the vertical orientation corresponds to the worst position for the receiver. Since the receiver is vertically oriented, the radiation beam propagates towards the direction parallel to the chest boundary, which is the closest to the receiver and, therefore, the region that contributes the most for the integral \( \Phi \). This behavior was also pointed out in [22] but, from the results shown in Fig. 4, it is possible to evaluate the difference between best and worst-case scenarios quantitatively. Namely, for the best positioning, the electric source presents an optimum frequency 590 MHz higher with a maximum \( \eta_E \) approximately five times the one verified with a vertically oriented source. A similar offset in efficiency magnitude can be verified between a horizontal and a vertical magnetic source. For lower frequencies, the best positioning leads to an efficiency around 2.5 times higher; however, the maximum difference between them surpasses 13 times in the far-field region.

It is also noticeable that the radiation efficiency behavior for an electric or magnetic receiver obtained with the realistic pectoral model agrees with those obtained with the simplified spherical model. Namely, for the horizontally oriented electric sources, \( \eta_E \) increases in the near-field range with a peak of 0.77% at 1.74 GHz, close to the optimum frequency shown in Table I for the same implantation depth of 37 mm, then decreasing for higher frequencies. In contrast, \( \eta_H \) reaches its maximum at lower frequencies, remaining almost constant around 10% in the near-field, before decreasing for frequencies above 1 GHz. The sharp reduction in radiation efficiency by a magnetic source in the far-field region is explained by the fact that this kind of source achieves its optimal performance as an electrically small antenna [43], [44], i.e., when \( L < \lambda/10 \) which is satisfied only in the near-field region.

As expected, there is a significant reduction in the maximum efficiencies obtained with the realistic model compared with the simplified spherical model. First of all, the latter considers a homogeneous medium equivalent to the human muscle tissue, whereas in the pectoral model, several organs with
different electromagnetic properties are taken into account. For this reason, two predominant loss sources are responsible for this efficiency deterioration: the increased attenuation, mainly in the fat and muscle layers where the power is dissipated before reaching the receiver in the heart; and the reflection losses due to the wave-impedance contrast between the medium that composes the tissues. In this last case, with the multiple reflections, most of the reflected power is dissipated in the tissue reducing the amount of power that reaches the receiver encapsulation. Therefore, this loss is accounted on $P_d$. Moreover, in a realistic scenario, the shape of the organs may lead to resonance modes responsible for local peaks and valleys in efficiency for some frequencies, such as 3.63 GHz for the electric source and around 1.74 GHz for the magnetic source.

IV. WPT EFFICIENCY AS A FUNCTION OF THE TRANSMITTER PARAMETERS

The case study of a wirelessly powered pacemaker is analyzed to establish the optimum parameters that lead to the maximum efficiency in a physically realizable application. In this case, the human pectoral model in Fig. 1 is used. However, the transmitter is now localized in the chest, as shown in Fig. 5. This transmitter comprises a substrate with the same dielectric properties as the medium external to the body and a lossless superstrate (or buffer) with thickness $d$ and relative electric permittivity $\varepsilon_b$. The electric transmitter in Fig. 5 is defined by assigning a surface current distribution $J_{Es}(x, y, z)$ given by:

$$J_{Es} = \begin{bmatrix} \cos \left( \frac{\pi x}{L} \right), 0, 0 \end{bmatrix},$$

in which $L$ is the transmitter length. Concurrently, the magnetic transmitter is modeled as a unitary out-of-plane electric current $I_{E} = 1$ A on the edge of the source with opposite phases, as illustrated in Fig. 5. As seen from the field distribution for the electric and magnetic transmitters, they are, for instance, equivalent to a dipole and loop antenna, respectively.

In this configuration, the two main transmitter parameters that can be changed to achieve the maximum wireless power transfer efficiency are the buffer thickness $d$ and its permittivity $\varepsilon_b$. Therefore, a parametric analysis was carried out for both parameters within the ranges: $1 \leq d \leq 50$ mm and $1 \leq \varepsilon_b \leq 80$. Furthermore, the lower and upper bounds for $\varepsilon_b$ were chosen so that this range comprises the permittivities of all nine tissues in the frequency spam from 100 MHz to 5 GHz. Consequently, the effective permittivity for this pectoral region is also in the chosen interval.

The operating frequency must be chosen and fixed to carry out this parametric study. Based on the results shown in Fig. 4, the maximum theoretical WPT efficiency for a deep-implanted pacemaker charged by an electric source transmitter is achieved at the frequency of 1.74 GHz. Considering the frequency bands allocated for Industrial, Scientific, and Medical (ISM) usage, the closest band to the optimal frequency is centered at 2.45 GHz. Henceforward, this is the frequency chosen for all following analysis, and the transmitter length $L$ was set as $\lambda/2$ at this frequency in free space.

In order to evaluate the wireless power transfer system for this configuration, (3) can be still be applied with the results from integrals (2a-2c); however, the integration domains need to be reformulated. In this case, $\Omega_s$ indicates that the integral is performed on the boundary of the pacemaker, whereas $\Omega_p$ represents the transmitter’s boundary.

Fig. 5. Analysis setup for the parametric analysis of the efficiency in a wireless powered pacemaker application: (a) close-up view of the on-body transmitter with length $L$ composed of a radiation source positioned apart from the skin by a lossless superstrate (buffer) with thickness $d$ and with a substrate matched to the medium external to the body. (b) Electric source modeled as a surface current density $J_{Es}$ with the electric field distribution indicated by the arrows and the magnetic field by the isolines. (c) Magnetic source modeled as an out-of-plane current $I_{E}$ with the magnetic field distribution indicated by the arrows and the electric field by the isolines.
The contour levels for the efficiency as a function of the buffer thickness and permittivity are shown in Fig. 6 for electric and Fig. 5 for magnetic sources. As it can be seen, the buffer parameters that lead to the maximum efficiency are \( d = 7 \) mm and \( \varepsilon_r^b = 80 \). The maximum efficiency is obtained with the highest permittivity can be explained once the wave-impedance mismatching at the transition buffer-skin is practically eliminated. In addition, taking into account this permittivity, the maximum occurs exactly at \( \lambda/2 \). As proved in [45], by considering the superstrate as a transmission line, it corresponds to the resonance condition, once the impedance seen in the transition transmitter-skin is equal to the impedance seen in the source, which leads to a high voltage at the source position, thus increasing the radiation efficiency. Moreover, it can be seen that as the buffer’s thickness increases, so decrease the optimum \( \varepsilon_r^b \) in such a manner that a \( \lambda/2 \) periodicity is obeyed, as it also happens with a lossless transmission line.

On the other side, the maximum efficiency obtained with a magnetic source is approximately an order of magnitude lower when compared with the electric one. It means that, at the frequency of 2.45 GHz, the magnetic source is sub-optimal, as it was also predicted in the graph of Fig. 4b, once it does not satisfy the electrically small antenna condition at this frequency. However, the maximum efficiency is achieved with \( d = 6 \) mm and \( \varepsilon_r^b = 46.5 \). It is important to mention that, in this case, this maximum occurs in a significantly narrow distance range, which in a practical realization would require precise positioning of the source.

In order to classify and quantify the losses, the optimal scenario in which the transmitter is composed of an electric source and a buffer with \( d = 7 \) mm and \( \varepsilon_r^b = 80 \) is considered. Three main loss mechanisms can be identified: reflection losses due to the wave impedance contrast between the on-body transmitter and the body tissue, antenna near-field losses, and the attenuation losses in the tissues. The two first losses can be mitigated by adequately designing the WPT system, whereas the latter cause is unavoidable. For instance, approximately 7% of the transmitted power is lost due to reflection in this optimum configuration, whereas 93% is due to attenuation and near-field losses combined. However, the optimal buffer parameters justify the low reflection losses and reduce the near-field region and its associated losses.

This fact raises a concern about the electromagnetic exposure levels for in-body WPT applications. The surface profiles for the local specific absorption rate (SAR) normalized by the transmitted power are shown in Fig. 7 for the optimal electric and magnetic sources. First of all, the SAR profiles follow the field distribution shown in Fig. 5b and Fig. 5c, being higher in the center for the electric source, whereas it reaches its maximum around the source edges for the magnetic. In addition, in both cases, the peak SAR is located in the skin layer, and no significant SAR values are observed in the vital organs. However, by comparing both SAR levels, it is noticed that the magnetic source leads to a larger SAR, almost twice the value for the electric source, even with much lower efficiency levels. Since the SAR is related to the attenuation in the tissues that cannot be physically mitigated, it is possible to conclude that the efficiency is maximized by properly choosing the transmitter parameters, and the electromagnetic exposure is minimized.

Finally, the fact that the efficiency obtained in this case is significantly lower when compared with the optimum efficiency presented in Fig. 4 shall be addressed. It can be explained by the fact that the transmitter is considered to be a conformal structure covering the entire body surface in the ideal scenario described in Section [III]. In contrast, the current analysis takes into account a mono-antenna transmitter, leading to a much smaller integration domain \( \Omega_p \), thus reducing the received power. In practical terms, it means that the single antenna mid-field WPT solutions currently in literature are sub-optimal by many orders of magnitude. Therefore, to physically achieve the maximum efficiency theoretically obtained, further developments in mid-field WPT are required based on conformal antenna arrays such as in [46] and techniques for electromagnetic focusing in lossy media that have already been
 investigates for other biomedical applications [47].

![Surface plot of the local specific absorption rate (SAR) in the region between the on-body transmitter and the deep-implanted receiver normalized by the transmitted power considering an optimal (a) electric and (b) magnetic source.](image)

**V. Conclusion**

In order to wireless power implantable bioelectronic devices, several techniques can be employed depending upon the application characteristics. However, the combination of different physical mechanisms imposes a limit to maximum achievable wireless powering efficiency. Among them, the principal mechanism is the electromagnetic attenuation in the dispersive tissues, the reflection losses, and the fundamental efficiency limitation of electrically small antennas. In addition to it, there are system-level losses and resonant modes in the body cavities that also contribute to efficiency deterioration. Therefore, this work focuses on evaluating the wireless powering efficiency of deep-body implanted devices and studying how the system’s parameters could be tuned to reach the highest efficiency possible in a practical application.

For this intend, a mathematical formulation for this problem was proposed based on reciprocity and T-symmetry principles as well as considering an on-body conformal source, perfectly matched to the human tissue. Such hypotheses lead to optimum energy focusing and, thus, to the highest possible efficiency. In order to validate this approach, a semi-analytical Spherical Wave Expansion analysis was carried out, and the results for a simplified spherical representation for the human body were compared.

This first analysis indicates that a magnetic receiver outperforms the electric one at the near-field frequency range, whereas, in the far-field, both receivers show similar performance. Therefore, the optimum frequency is in the mid-field region and depends upon the source type and implantation depth, leading to the highest efficiency.

Once the proposed approach was validated, it was applied to an anatomical model focused on a deep-implanted wireless powered pacemaker application [16]. This analysis verified that the overall behavior for both sources agrees with the one predicted by the simplified spherical model, including the optimum operation in the mid-field range. Furthermore, this optimum frequency also agrees with the results presented in literature obtained through different approaches [22], [23], [25]–[29]. Even though there is a significant efficiency reduction in the realistic model results, it is because now the wave impedance contrast between the different tissues imposes reflection losses that were disregarded in the simplified model. Moreover, with this model, it was verified that the receiver orientation is another practical aspect that can reduce efficiency. Considering the source positioning, the maximum difference in efficiency between the best and worst-case scenarios is around five times for an electric receiver, whereas, for the magnetic one, this difference can be above 13 times. The effect of the source orientations is justified once in the best case, i.e., for a horizontally oriented receiver, the power flows towards the chest line, which is the closest point to the receiver, contributing more for the overall received power. It is important to mention that the flexibility in analyzing different source types is another contribution of the proposed approach compared to other methods of analysis.

Finally, a wireless power transfer system considering a deep-implanted pacemaker as the receiver and a multilayered (substrate-source-buffer) transmitter positioned in the chest was considered to analyze the impact of the transmitter’s parameters on the powering efficiency as well as to provide information on how these parameters could be tuned in order to achieve the maximum efficiency. This parametric study has shown that at the 2.45 GHz ISM band, the electric transmitter leads to efficiency over a degree of magnitude higher than a magnetic one. In addition, the maximum efficiency can be achieved with a lossless high-permittivity buffer, matched to the skin permittivity, and thickness equal to $\lambda/2$ in this medium. Furthermore, other local maxima can be obtained for thicker and lower permittivity superstrates, respecting a $\lambda/2$ periodicity.

To summarize, the approach proposed in this paper is able to predict the maximum achievable powering efficiency considering simplified or anatomical body models as well as to provide information on the parameters that can be optimized in order to achieve this maximum efficiency. In addition, even though the case study of a deep-implanted pacemaker was analyzed in this paper, the same approach could also be used to evaluate the powering efficiency for other deep-body implantable devices.

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