THE VELOCITY OF THE EMITTING PLASMA OF
THE SUPERLUMINAL GALACTIC SOURCE GRS 1915+105

Gianluigi Bodo and Gabriele Ghisellini
Osservatorio Astronomico di Torino
Strada Osservatorio, 20 10025 Pino Torinese, Italy

ABSTRACT

We calculate the flux and size ratio of radio emitting features moving in antiparallel
directions at relativistic speeds, taking into account that the pattern we observe may
move at a velocity different from the one of the emitting plasma. Both velocities can
be determined in sources in which both the approaching and the receding features are
observed. This is the case of the galactic superluminal source GRS 1915+105, for which
the pattern speed (responsible for the apparent superluminal velocity) was found to
be 0.92\(c\). For this source we find that the velocity of the plasma is 0.73\(c\). The found
velocity helps decreasing the estimate of the associated kinetic power. Since intrinsically
identical knots will be observed to have different sizes, high resolution radio observations
of GRS 1915+105 will be a test for the proposed difference of the pattern and plasma
velocities.

Subject headings: Relativity – Radio continuum: stars — Stars: GRS 1915+105

1. INTRODUCTION

Two oppositely directed blobs of radio emission have been recently observed to move at
relativistic speeds in GRS 1915+105 (Mirabel & Rodriguez, 1994, hereinafter MR94).
The apparent velocities are \(\beta_a = 1.25\pm 0.15\) and \(0.65\pm 0.08\): one of the blobs is therefore
superluminal. This is the first example that the violent phenomena occurring in active
galactic nuclei (AGNs) may be reproduced on a much smaller scale also by objects in
our own galaxy. Due to the proximity of this source, probably located at 12.5 Kpc from
us, we have a unique opportunity to study relativistic effects in much greater depth than
what is possible for AGNs. Indeed, GRS 1915+105 is the first example of superluminal
source in which we can observe a pair of blobs going away from a stationary center. This
has already allowed MR94 to determine both the real velocity of the moving patterns and the angle of motion with respect to the line of sight. Using the derived ‘true’ speed ($\beta = 0.92 \pm 0.08$) and viewing angle ($\theta = 70^\circ \pm 2^\circ$), MR94 were also able to estimate the total emitting mass, the kinetic energy of its bulk motion, and the corresponding kinetic power, which turned out to be worryingly large: $L_{\text{kin}} \sim 10^{41}$ erg $s^{-1}$. Furthermore, the knowledge of $\beta$ and $\theta$ immediately lead to the prediction of the expected frequency shift of any emission line, whose detection would be, of course, very important to confirm our ideas about beaming models.

In this Letter we will argue that the ‘true’ velocity of the emitting plasma can (and very likely is) lower than the velocity of the moving pattern responsible for the apparent superluminal speed. This will partly ease the problem in explaining the large kinetic power and allows to make a more detailed prediction of the frequency shift of the emission line by the outflowing matter. The above results are largely model independent. We also calculate the apparent sizes of the approaching and receding knots, and discuss how their ratio can give further independent informations on the pattern and plasma velocities.

2. OPPOSITELY MOVING BLOBS

2.1 FLUX RATIO

In this section we offer a simple derivation of the expected flux density from two blobs moving in antiparallel directions. The pattern of each blob is moving at some velocity $\beta_s$, while the velocity of the fluid inside each blob is moving with a different velocity $\beta_F$. All velocities are measured in the observer frame, and the angle $\theta$ is between the line of sight and the velocity of the approaching blob. As a special case, we may have $\beta_s = \beta_F$ (the plasmon case), for which the observed optically thin flux ratio is (for power law emission $F(\nu) \propto \nu^{-\alpha}$)

$$\frac{F_a(\nu)}{F_r(\nu)} = \left(\frac{1 + \beta \cos \theta}{1 - \beta \cos \theta}\right)^{3+\alpha}, \quad (\beta = \beta_s = \beta_F) \quad (1)$$

here the subscripts $a$ and $r$ stand for approaching and receding, respectively.

In the more general case of $\beta_s \neq \beta_F$, we have to integrate the emissivity (as it is in our observer frame) over the observed volume. It is of course better to express the emissivity in a frame comoving with the emitting plasma (comoving quantities will be denoted by a prime), using
\[ j_{a,r}(\nu) = \left[ \frac{1}{\gamma_F (1 \pm \beta_F \cos \theta)} \right]^{2+\alpha} j'_{a,r}(\nu) \equiv \delta^{2+\alpha}_{j'_{a,r}} j_{a,r}(\nu) \]  

where \( \delta_F \) is the Doppler factor of the fluid. A simple way to derive the above transformation is to write \( j(\nu) \) as the number of photons of energy \( h\nu \) emitted per unit time, frequency, solid angle and volume, i.e. as \( \propto dN/h\nu/(dt d\nu d\Omega dV) \) and Lorentz transforming all the quantities (i.e. Rybicki & Lightman, 1979).

What is the observed volume? When we make a flux measurement (or a map) we collect photons arriving at the same time to the detector. For extended objects, therefore, these photons left the source at different times (Terrel, 1960). For the approaching blob, the photons emitted at the back of the blob have to leave at earlier times than the photons emitted at the front. This time interval corresponds also to different locations of the blob, whose front moves with the pattern velocity \( \beta_s c \). The reverse is true for the receding blob. The ratio of the approaching and receding volumes is

\[ \frac{V_a}{V_r} = \frac{1 + \beta_s \cos \theta}{1 - \beta_s \cos \theta} \]  

Therefore the ratio of the observed fluxes is

\[ \frac{F_a(\nu)}{F_r(\nu)} = \frac{1 + \beta_s \cos \theta}{1 - \beta_s \cos \theta} \left( \frac{1 + \beta_F \cos \theta}{1 - \beta_F \cos \theta} \right)^{2+\alpha} \]  

Special cases are:

i) \( \beta_s = \beta_F \). Then equation (4) reduces to equation (1).

ii) \( \beta_s = 0 \). This is the case of a stationary jet, whose volume is fixed in the observer frame.

iii) \( \beta_F = 0 \). This is the case of antiparallel perturbations travelling along the jet, powering different portions of plasma at rest (or slowly moving). Even in this case the flux ratio is greater than unity, and can reach large values for small angles.

The same result (i.e. equation 4) can be derived by using the formalism of Lind & Blandford (1985), in particular using their equation (2.12b), but we think that our derivation is simpler and readily applicable to the case of superluminal sources in which both approaching and receding blobs are observed, as is the case of GRS 1915+105.

2.2 SIZE RATIO

Two oppositely moving blobs, identical in their rest frame, will have different sizes in the observer frame. For illustration, consider the case of two cylinders of heigth \( l \) and
section diameter $d$, measured in its proper frame, moving at velocities $\pm \beta_s$ along a
direction which makes an angle $\theta$ with the line of sight. When we compute its projected
length seen by the observer, we have to take into account aberration, time delay and
Lorentz contraction effects. We note that, as in the previous discussion, the projected
length is that defined by the photons collected at the same time by the observer, which,
therefore, left the source at different times. The total length observed is made by two
contributions, the projected height and the projected section of the cylinder. The first
one, being parallel to the velocity is modified by Lorentz contraction and time delay
and becomes

$$l^{\text{obs}} = l \sin \theta \frac{1}{\gamma_s} \frac{1}{1 - \beta_s \cos \theta} = l \delta_s \sin \theta$$  \hspace{1cm} (5)

For the second one we have only to consider time delay effects, and we have

$$d^{\text{obs}} = \frac{|\cos \theta - \beta_s|}{1 - \beta_s \cos \theta} d$$ \hspace{1cm} (6)

We note that, when $\beta_s < \cos \theta$, we see the face of the cylinder closer to us, when
$\beta_s = \cos \theta$, the projected size of the section of the cylinder is zero and we see only its
lateral surface, while, when $\beta_s > \cos \theta$, we see its farther face.

The total projected length is $l^{\text{obs}} + d^{\text{obs}}$ and the ratio between that observed for
the approaching cylinder and that observed for the receding one is

$$R = \frac{\sin \theta + x \gamma_s |\beta_s - \cos \theta| 1 + \beta_s \cos \theta}{\sin \theta + x \gamma_s (\beta_s + \cos \theta) 1 - \beta_s \cos \theta},$$ \hspace{1cm} (7)

where $x = d/l$. The same result could be obtained considering the invariance of the
perpendicular separation between two parallel light rays (see e.g. the discussion after
equation 2.6 of Lind & Blandford 1985). Using this method the observed total length
can be obtained by the following procedure: i) calculate the aberration angle relative
to the observer and the proper frame; ii) in the proper frame, consider the direction
of the ‘de–aberrated’ rays; iii) project the cylinder (in the proper frame) in a plane
perpendicular to the this direction. This is the projected shape seen by the observer.
Using this method is immediately apparent that the maximum length of a fast moving
object cannot be larger than the maximum length seen in the proper frame projecting
the object in different directions. (i.e. the maximum length of a cylinder is $\sqrt{d^2 + l^2}$).

In a real situation we can imagine that the cylindrical regions observed are asso-
ciated to shocks and correspond to the regions of emitting post–shock material. Their
length will therefore be determined by the cooling time of the post–shock material and
will be in general a function of the frequency of observation. Defining the post–shock
plasma velocity, in the shock frame, as $\beta_s^F$ and its cooling time, in the plasma proper frame, as $t_{cool}^F(\nu^F)$, we can compute the cooling length in the shock frame as

$$l_{cool}^s = ct_{cool}^F(\nu^F)\gamma_s^F \beta_s^F$$

In the previous and following expressions the superscripts $F$, $s$ denote quantities measured respectively in the shock and plasma frames. To find how the cooling time depends on frequency, we must assume a given emission mechanism. For synchrotron $t_{cool}(\nu) \propto \nu^{-1/2}$ which yields $t_{cool}^F(\nu^F) = t_{cool}^F(\nu)\delta_F^{1/2}$, where $\nu$ is the observed frequency. Expressing now $\beta_s^F$ and $\gamma_s^F$ in term of the plasma and shock velocities seen by the observer and using the observed frequency, we obtain the following expression for the quantity $x$ appearing in Eq. (7):

$$x(\beta_s, \beta_F, \theta, \nu) = \frac{d}{ct_{cool}^F(\nu)\delta_F^{1/2} \gamma_s \gamma_F (\beta_s - \beta_F)} \quad (9)$$

Special cases are:

i) $\beta_s = \beta_F$: in this case equation (7) yields $R = \sqrt{(1 + \beta_s)/(1 - \beta_s)}\cos \theta - \beta_s/(\cos \theta + \beta_s)$, which is always less than unity.

ii) $d \ll ct_{cool}^F$: in this limiting case $R = (1 + \beta_s \cos \theta)/(1 - \beta_s \cos \theta)$, independently on the fluid velocity, reaching very large values for small viewing angles.

iii) $\beta_F = 0$: even in this case we expect $R$ to be, in general, different from unity, especially at small viewing angles.

3. APPLICATION TO GRS 1915+105

As measured by MR94, the flux ratio of approaching and receding blobs in GRS 1915+104, calculated at equal separations from the center (hence when the blobs have the same age) is $\sim 8 \pm 1$, inconsistent with the value ($F_a/F_r \sim 12$) expected in the case of equal pattern and fluid velocities. Using our equation (4) with $\beta_s = 0.92$ and $\theta = 70^\circ$, we derive $\beta_F = 0.73$ assuming a flux ratio equal to 8 (it becomes 0.664 and 0.787 with flux ratios equal to 7 and 9, respectively), corresponding to a Lorentz factor $\gamma_F = 1.46$.

Any line emitted by the moving fluid would be shifted in frequency by $\delta_{F,a} = 0.911$ (approaching fluid) and by $\delta_{F,r} = 0.547$ (receding fluid), which are significantly different by the values found using $\beta = 0.92$ and quoted in MR94.

With the derived value of $\beta_F$ we can predict the size ratio $R$ as a function of $x(\nu)$, which is unfortunately unknown. However, for $x(\nu) = 0, 1$ and 100 we have $R = 0.92,$
0.84 and 0.68, respectively. Even if the precise value of $x(\nu)$ is not known, a well defined behaviour of $R$ is predicted: $R$ should decrease by observing at different, increasing, frequencies, which correspond to shorter cooling times and therefore at larger $x(\nu)$.

Also the estimate of the kinetic power will be significantly affected. In fact, in order to estimate the total mass producing the synchrotron emission we observe, we have to correct the observed luminosities and frequencies with the correct Doppler factor. Following MR94, we may approximate the energy distribution of the emitting particles with a monoenergetic function at $\gamma = 10^{\gamma_3}$, a typical value to produce an observed frequency of $10\nu_{10}\delta$ GHz. This fixes a fiducial value for the magnetic field $B = 2.7 \times 10^{-3} \nu_{10}\delta/\gamma_3^2$. Charge neutrality may be provided by protons or positrons. Since electron and positrons would have the same large $\gamma$ while protons are very likely not relativistic, the hypothesis of a pure pair plasma would only slightly affect (factor 2) the mass estimate.

With the values of $\delta$ derived above, we obtain a new estimate for the total mass of $M = 7.6 \times 10^{24}$ g, a factor 3 lower than MR94. The kinetic luminosity is $L_{\text{kin}} = 2.6 \times 10^{40}$ erg s$^{-1}$, a factor $\sim 4$ lower than MR4.

**DISCUSSION**

Superluminal sources in which both the approaching and the receding blobs are observed offer the opportunity to estimate both the velocity of the pattern and the velocity of the emitting plasma. For the recently discovered galactic source GRS 1915+105 the estimated plasma velocity is $\beta_s = 0.73 \pm 0.06$, significantly lower than the pattern speed $\beta_s = 0.92 \pm 0.08$.

This velocity difference is suggestive of a shock propagating along the jet with velocity $\beta_s$ and postshock velocity $\beta_F$. The velocity difference found would indicate a compression ratio lower than that expected for strong relativistic shocks in a non-magnetized medium. Our result is therefore indicative that the magnetic field is likely to be important for the dynamics of the flow observed in this source, however more precise conclusions are precluded by the uncertainties in the relativistic shock theory (Appl & Camenzind 1988).

If the moving knots are not spheres, as our analysis implies, than their apparent, projected shapes are modified by Lorentz contraction and by the different travelling times of the photons emitted in different part of the source. This modifications are different for the approaching and the receding knots, in such a way that two intrinsically
(when at rest) equal knots are observed to have a different total projected size.

With sufficient angular resolution, the approaching and receding blobs of GRS 1915+105 should not be observed as circles of equal diameters, but with elongated patterns of different maximum extension. The ratio of their sizes can confirm or not the plasma velocity derived from the flux ratio.

As mentioned, any line emitted by the plasma should be observed shifted in frequency, immediately giving (for a given angle) the corresponding velocity. Formation of lines could however be strongly inhibited in a too hot gas. An attractive alternative is the annihilation line, expected if part of the jet material is made by electron–positron pairs. Note that the source 1E1740–294, close to the galactic center, is thought to have jets carrying electron–positron pairs, to explain the variable annihilation line observed by the SIGMA satellite (Bouchet et al. 1991, Sunyaev et al. 1991, Ramaty et al. 1992). GRS 1915+105 may be similar. We may very roughly calculate an upper limit to the annihilation line flux assuming that all the particles emitting in the radio, once cooled, annihilate before escaping the source. These particles, of initial energy $\gamma_0$, emit a fraction $(\gamma_0 - 1)/\gamma_0$ of their total energy as radio emission, and a fraction $1/\gamma_0$ as annihilation radiation. Therefore $F_{\text{ann}} \sim F_{\text{radio}}/\gamma_0$ corresponding to a photon flux $\dot{N} \sim 10^{-7} \nu_{10} F_{Jy}(\nu_{10})/\gamma_0$ [photons cm$^{-2}$ s$^{-1}$]. This limit can be increased if only a fraction of the existing pairs have been accelerated to high energies to radiate in the radio. In this case one can obtain another upper limit by considering that the nucleus of the source transforms a fraction $\xi$ of its hard X–ray luminosity into pair rest mass. The maximum value of $\xi$ is thought to be around 10 per cent (Svensson, 1987) for non thermal plasmas, and much less for thermal ones. In this case, the estimated limit for the annihilation photon flux is $\dot{N} \sim 6.5 \times 10^{-3} \xi L_{38}$ [photons cm$^{-2}$ s$^{-1}$], where $L_{38}$ is the luminosity in hard X–rays in units of $10^{38}$ erg s$^{-1}$.

REFERENCES

Bouchet L. et al., 1991, ApJ, 383, L45
Lind, K.R. & Blandford, R.D., 1985, ApJ, 295, 358
Mirabel, I.F. & Rodriguez, L.F., 1994, Nature, 371, 46 (MR94)
Ramaty, R., Leventhal, M. Chan, K.W. & Lingenfelter, R.E., 1992, ApJ, 392, L63
Rybicki, G.B. & Lightman A. P., 1979, Radiative Processes in Astrophysics, ed John Wiley & Sons (New York)
Sunyaev, R. et al., 1991, ApJ, 383, L49
Svensson, R., 1987, MNRAS, 227, 403
Terrel, J., 1959, Phys. Rev., 116, 1041