Solitonic excitations in collisions of superfluid nuclei

a qualitatively new phenomenon distinct from the Josephson effect

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Abstract. Recently, we have reported a novel role of pairing in low-energy heavy ion reactions at energies above the Coulomb barrier, which may have a detectable impact on reaction outcomes, such as the kinetic energy of fragments and the fusion cross section [arXiv:1611.10261, arXiv:1702.00069]. The phenomenon mimics the one studied experimentally with ultracold atomic gases, where two clouds of fermionic superfluids with different phases of the pairing fields are forced to merge, inducing various excitation modes of the pairing field. Although it originates from the phase difference of the pairing fields, the physics behind it is markedly different from the so-called Josephson effect. In this short contribution, we will briefly outline the results discussed in our recent papers and explain relations with the field of ultracold atomic gases.

1 Introduction

Although, almost 60 years have passed after the seminal work by A. Bohr, B.R. Mottelson, and D. Pines [1] that pointed out the existence of the pairing correlations in atomic nuclei, the pairing dynamics in low-energy heavy ion reactions still remains as one of the open problems in nuclear physics. On the analogy of the so-called Josephson effect occurring between superconducting metals [2], researchers envisaged analogous effects, referred to as nuclear Josephson effect, leading to subbarrier nucleon-transfer processes in collisions of two superfluid nuclei [3–6]. Nowadays simulations of heavy ion reactions based on microscopic time-dependent mean-field theories including pairing correlations have become possible, providing valuable insights into the problem [7–10], owing to the continuous increase of computation power. We should note, however, that numerical simulations of nuclear reactions based on full time-dependent Hartree-Fock-Bogoliubov (TDHFB) theory have been achieved, only very recently [11]. It can be expected that now the time is ripe enough for elucidation of qualitatively new phenomena associated with dynamical effects of pairing in low-energy heavy ion reactions.

Due to collaborations of nuclear theory groups at the University of Washington and Warsaw University of Technology, a theoretical framework, which utilizes a local treatment of time-dependent density functional theory (TDDFT) including superfluidity, has been extensively developed. It has been shown that the approach, named time-dependent superfluid local density approximation (TDSLDA), is a powerful tool for accurately describing complex dynamics of strongly-correlated fermionic systems, like ultracold atomic gases [12–18] and nuclear systems [19–23]. In our recent papers [24, 25], we have extended the application of TDSLDA to low-energy heavy ion reactions, employing FaNDF\textsuperscript{0} nuclear functional [26, 27] without spin-orbit coupling, and found a qualitatively new phenomenon associated with the pairing field dynamics in collisions of two superfluid nuclei.

In Refs. [24, 25], we have reported the results of TDSLDA simulations for \(^{44}\text{Ca}+^{44}\text{Ca}, \(^{90}\text{Zr}+^{90}\text{Zr}, \(^{96}\text{Zr}+^{126}\text{Sn}, \) and \(^{240}\text{Pu}+^{240}\text{Pu}\) reactions at various incident energies (note that neutrons in \(^{90}\text{Zr}\) are in superfluid phase without spin-orbit coupling). It has been shown that a soliton-like excitation mode emerges inside the neck region, in which pairing vanishes, when two superfluid nuclei possessing different phases of the pairing field collide. The situation resembles the one encountered in experiments with ultracold atomic gases, where two clouds of superfluid atomic gases are forced to merge, creating a solitonic excitation (domain wall) which decays through quantum vortices [28, 29]. From the results, it has been shown that the solitonic structure is relatively long-lived object that stays until the composite system splits. Because of this fact, the solitonic excitation effectively hinders energy dissipation from translational motion to internal degrees of freedom as well as the neck formation, resulting in dramatic changes of the reaction dynamics (see Refs. [24, 25] for more details).

In Fig. 1, we show one of the illustrative examples of our TDSLDA simulations for the \(^{90}\text{Zr}+^{90}\text{Zr}\) reaction at \(E \approx 1.05\text{V}_{\text{Bass}}\), for two extreme cases: \(\Delta \varphi = \pi\) and \(\Delta \varphi = 0\), which are shown in upper-half and lower-half of each panel of the figure, respectively. Here, \(\Delta \varphi\) denotes...
the relative phase difference of the pairing fields of colliding superfluid nuclei. Snapshots of the total density on the reaction plane at various times are shown in the left column, while those of the absolute value of the neutron’s pairing field are shown in the right column. Since the collision energy is higher than the Coulomb barrier, two nuclei collide clearly showing a substantial overlap of the density (see the left column). However, in the $\Delta \varphi = \pi$ case (upper-half), two nuclei do not fuse and eventually reseparate generating binary reaction products; whereas the $\Delta \varphi = 0$ case (lower-half) resulted in fusion.

What makes the dynamics so different? The answer lies in the dynamics of excitation modes of the pairing field, which is depicted in the right column of the figure. From the figure, one can clearly see that a narrow region in which the pairing field vanishes is created on the course of collision in the $\Delta \varphi = \pi$ case (upper-half), which we refer to as solitonic excitation of the pairing field. Since the phase changes so steeply between the colliding nuclei, the system chooses to become normal inside the solitonic structure. The solitonic excitation prevents the system to form a compact (mononuclear) shape (see left column) and, as a result, fusion reaction is hindered, even though the system once overlapped substantially (Note that there is a remarkable difference compared to a lighter system, where two nuclei easily get fused once the system overlapped only slightly [25]). Summarizing, from our comprehensive simulations, we have found that [24, 25]: total kinetic energy (TKE) of outgoing fragments can be changed as large as 25 MeV in $^{208}$Pb+$^{208}$Pb; fusion threshold energy can be affected almost 30 MeV in $^{90}$Zr+$^{90}$Zr, similar effects present also for an asymmetric system, $^{66}$Zr+$^{126}$Sn; whereas the pairing effects turned out to be small in a lighter system, $^{44}$Ca+$^{44}$Ca, because of the strong tendency towards fusion, consistent with an earlier study [11].

Although the effect originates from the relative phase difference of the pairing fields of two colliding superfluid nuclei, it is not related to the Josephson effect. As we feel that it would be useful to clarify the distinct character of the effect we studied, as compared to the Josephson effect, we explain this point in detail.

2 Solitonic excitation vs Josephson effect

Let us first remind that the physics of the Josephson effect deals with the phenomenon of the current flowing through a junction in the absence of the chemical potential difference. The first Josephson’s paper on the subject entitled “Possible new effects in superconductive tunnelling” [2] states clearly in the introduction that: “We here present an approach to the calculation of tunneling currents between two metals that is sufficiently general to deal with the case when both metals are superconducting. In that case new effects are predicted, due to the possibility that electron pairs may tunnel through the barrier leaving the quasi-particle distribution unchanged”.

This current, being only dependent on the mutual phase differences of the pairing fields, is responsible for a variety of effects which are known under a common name of “Josephson effect”. However, the crucial point is that

$$J(t) = \mathcal{J}_c \sin[\Delta \varphi(t)],$$

$$\frac{d(\Delta \varphi)}{dt} = \frac{eU}{h},$$

where $\mathcal{J}_c$ is the amplitude of the Josephson current, $e$ is the elementally charge, $h$ is the reduced Plank constant, and $U$ is the voltage, which, in nuclear case, will be proportional to the chemical potential difference. Thus, sub-barrier multinucleon transfer processes between superfluid nuclei can be viewed as a nuclear Josephson effect and papers [3–6] focused solely on this aspect.

However, we would like to emphasize here that the Josephson effect described above is markedly different from the effect we studied in Refs. [24, 25]. What we investigated is collisions of superfluid nuclei at energies above the Coulomb barrier, which, on the contrary to the Josephson effect, can be regarded as a strong-coupling limit, where two condensates (nuclei) actually merge producing a solitonic excitation (domain wall). Both effects are associated with the pairing field, but are weakly connected in the sense that: no solitonic excitation is necessary for the Josephson current to appear; whereas no
Josephson current is necessary for the effect we studied to appear. Indeed, we have shown that the strongest effect is observed actually for the $\Delta \phi = \pi$ case where no Josephson current is present. [24, 25]. Usually the Josephson effect is studied in the regime of a quasistationary situation, which occur when two condensates couple weakly through the potential barrier, and therefore no topological excitation of the pairing field (soliton or quantum vortex) is expected. In our case, on the other hand, we studied rather violent collisions at energies above the Coulomb barrier, i.e., far from the stationary situation, which trigger the appearance of the localized excitation mode between colliding super-fluid nuclei.

To emphasize better the differences between the Josephson effect and the effect that we studied in our papers [24, 25], let us consider the system where both phenomena can be studied with far better accuracy than in nuclear systems. Namely, let us consider the case of ultra-cold fermionic (atomic) gases. In the latter case, studies of the Josephson effect can be achieved experimentally. The current is realized as a tunneling between two fermionic superfluids separated by an external potential barrier. In Fig. 2 (left), we show a typical experimental setup, which allows to investigate a Josephson alternating current due to the weak coupling of two Lithium atomic clouds [31].

As a result an oscillatory current is observed accompanied with an oscillatory evolution of the phase difference between the condensates [see Fig. 2 (right)]. For the flow of the atoms the weak coupling is sufficient and no solitonic excitation is present.

On the other hand, the effect we studied is more closer to the experiments performed by the MIT group [32–34], which consist in merging two atomic clouds with different phases and producing topological excitations (see Fig. 3). There is no external potential that separates the cloud at all. Note that this phenomenon, although originating from the pairing field dynamics, is not related to the Josephson effect. The reason is that in this case physics is different, although of course certain flow of particles induced by the pairing field is observed. However, the main feature comes from the nonlinear evolution of the pairing field, which makes the solitonic excitation relatively long lived. With TDSLDA approach, we were able to successfully simulate this experiment and we found that in case of the unitary Fermi gas the excitation decays into a vortex ring [35], which is another type of the topological excitations of the pairing field. This prediction was confirmed by the experiment in Ref. [34].

We understand that in nuclear physics community this distinction has not been emphasized, since all papers,
which concern physics of colliding superfluid nuclei, have investigated only the consequences of the supercurrent (or pair transfer) which would manifest in multinucleon transfer processes in heavy ion reactions. Indeed, this effect has been studied, but it is relatively weak and has nothing to do with the phenomenon we studied in Refs. [24, 25]. The latter requires not only the phase difference but also the creation of the solitonic structure which stays relatively long so as to hinder energy dissipation and the neck formation during the collision. In other words, the Josephson effect originates from the weak coupling between two condensates separated by a potential barrier, whereas in our case we consider a strong coupling limit where two condensates actually merge/collide. It would be misleading to refer to the latter as the effect that is already known from the weak coupling limit, in the same way, like it would be misleading to say that properties of a turbulent flow are known because a laminar flow has been studied. Analogously, physics of a weakly-interacting Fermi gas described by the standard Bardeen-Cooper-Schrieffer (BCS) theory is completely different from the one in the strong coupling limit (i.e. for the unitary Fermi gas) where a variety of qualitatively new phenomena occur like, e.g., pseudogap or anomalously small ratio of the shear viscosity to the entropy density. One cannot say that the unitary Fermi gas is a well-known system because it is a superfluid just like a typical atomic nucleus.

3 Summary

In our recent papers [24, 25], we have reported a qualitatively new phenomenon in low-energy heavy ion reactions at energies above the Coulomb barrier, which is associated with relative phase difference of the pairing fields of colliding superfluid nuclei. We have found that the complex pairing field dynamics may substantially alter the reaction outcomes, such as the total kinetic energy of the fragments and the fusion cross section, which may be experimentally detectable for carefully selected systems. In our simulations, a “solitonic excitation” (domain wall) is observed in the neck region, inside which pairing vanishes, resulting in hindrance of energy dissipation as well as the neck formation, leading to significant changes of the reaction dynamics. Although this effect originates from the relative phase of the pairing fields of colliding superfluid nuclei, the physics behind it is markedly different form the so-called Josephson effect: the latter is associated with a weak coupling of condensates (separated by a potential barrier) without any solitonic excitation, whereas the effect we studied is associated with a strong-coupling limit where two condensates are actually merge/collide for which no Josephson current is necessary. The ongoing further extensions and applications of the present work will enable us to find qualitatively new phenomena associated with the pairing field dynamics that have never been investigated in nuclear physics community.

Acknowledgments

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pairing field dynamics that have never been investigated in tensions and applications of the present work will enable Josephson current is necessary. The ongoing further examination, leading to significant changes of the reaction dynamics. Although this effect originates from the relative difference of the pairing fields of colliding superfluid nuclei, the physics behind it is markedly different. The latter is associated with a weak-coupling limit, in the same way, like it would be misleading to refer to the standard Bardeen-Cooper-Schrieffer (BCS) theory as the latter as the effect that is already known from the weak-coupling limit, whereas the effect is called Josephson effect: the latter is associated with a weak-coupling limit (BCS) theory is completely different from the coupling limit, in the same way, like it would be misleading to refer to the standard Bardeen-Cooper-Schrieffer (BCS) theory is completely different from the coupling limit.

In our recent papers [24, 25], we have reported a qualitatively new phenomena occur like, e.g. pair transfer) which would manifest in multinucleon trans-
crations, such as the total kinetic energy of the fragments.

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