Cox Proportional Hazard Survival Analysis to Inpatient Breast Cancer Cases

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Abstract: Breast cancer problems are characterized by increased incidence and trends, including death. The prognosis of survival rate in 5 years in stadium I is 90%, stadium II 65%, stadium III 15-20%, and stadium IV is less than 5%. To determine survival rate and cause of death, survival analysis has been done to find the relationship between survival rate and clinical stages, tumor location, metastasis, age and co-morbidity. A retrospective cohort study of inpatient breast cancer cases in Ibnu Sina UMI Hospital, Makassar, Indonesia 2013-2016 was selected as 108 cases out of 436 all inpatient cases. The survival analysis was performed using Kaplan-Meier and Cox Proportional Hazard methods. The results showed that the survival probability was 0.029, and the median survival was 20 months at intervals from 0 to 46 months. Significant related factors with survival rate were metastasis and co-morbidity. The Hazard Ratio of cancer stadium II dan III was 2.061 and hazard ratio of cancer stadium IV was 1.571. Moreover, Stadium III survival rate was 73.1%, and stadium IV / metastases decreased to 6.5%, but it was increased to 42.6% when treated. Suggestion of the need for early detection of breast cancer, so women should come early to visit health facilities.

1. Introduction

Breast cancer is a very dangerous disease that spreads all over the world. [1]. Breast cancer gets a lot of doctors and statisticians' attention because it has a high mortality rate with an unstable tendency to death, with numerous and varied prognostic factors [1] [2]. The presence of breast cancer in Indonesia ranks first with a prevalence of 0.5 per 1,000 women. In addition to the high prevalence, breast cancer problems are characterized by high mortality, associated with late diagnosis or patients coming for treatment when it goes to advanced stage [3] [4]. Classification of breast cancer stage according to AJCC [5] has a relationship with survival prognosis. This situation is indicated by decreasing survival rate from Stage I 90%, Stage II 65%, Stage II 20% and Stage IV 5% [6]. To determine why the survival rate of breast cancer cases is low, it is necessary...
to identify the prognostic factors survival rate [7]. The major prognostic factors of breast cancer are associated with several possible approaches to diagnosis, including clinic stages [8], and histopathological grade [9] [10]. Survival rate depends also on the type of diagnosis based on the existence of metastasis [11-13]; radiologic figure of mammography [14]; and genetic expression [15]. In addition to the clinical stage stage of breast cancer or the type of diagnosis, there are several other prognostic factors associated with survival rate, namely: age [16], race [15], co-morbidity: diabetes [18]; anemia [7] [19], family history [7], tumor size [20] [21], location of lymph node metastasis [11] [21]. Survival rate is also related to type of surgery and treatment, including in chemotherapy [22], breast surgery [23], hormonal [7] and radiotherapy [24].

Therefore, this study will analyze the prognostic factors associated with survival rate of breast cancer patients. Based on breast cancer condition, especially in predicting the important prognostic factors, statistician could used survival analysis, which have several models. One of most commonly used model is Cox proportional hazard with Kaplan-Meier and Log-Ranks test [24] [25] [26-28].

2. Methods and Materials

2.1 Study Design

Learning is A retrospective cohort study of inpatient breast cancer cases in IbnuSina UMI Hospital, Makassar, Indonesia 2013-2016 was selected as 108 cases out of 436 all inpatient cases. The survival analysis was performed using Kaplan-Meier and Cox Proportional Hazard methods [29] [30]. Kaplan-Meier model was used to determine survival probability of breast cancer patients. Then, Log-Rank test was used to determine the significance difference between survival expression of the patient [26]. Cox proportional hazard was used to determine the difference ratio of prognostic factors which were including age, clinical stages, tumor size, location of lymph node metastasis, and co-morbidity [31].

2.2 The Survival Function

Individual opportunities to survive for time x are expressed by \( S(x) = P(X > x) \). Let \( X \) be the continuous random variables, then the survival function is the complement of the cumulative distribution function \( S(x) = 1 - F(X) \) where \( F(X) = P(X \leq x) \). The survival function is the integral of the probability density function \( f(x) \):

\[
S(x) = P(X > x) = \int_{x}^{\infty} f(t)dt \quad (1)
\]

\[
f(x) = -\frac{dS(x)}{dx} \quad (2)
\]

Then if \( X \) is the discrete random variables, and can be obtained \( x_{j}, j=1,2,3,... \) with the probability mass function (p.m.f) \( p(x_{j}) = P(X = x_{j}) \), \( j=1,2,3,... \) where \( x_{1} < x_{2} < x_{3} ... \) then the survival function for the discrete variables \( X \) is given by:

\[
S(x) = P(X > x) = \sum_{x_{j} > x} p(x_{j}) \quad (3)
\]

2.3 Hazard Functions

The hazard function of the hold time \( X \) is denoted by \( h(x) \) and defined as individual probability fails in the time interval \( (x,x+\Delta x) \) that the individual has lived for time \( x \), the hazard function is expressed as:

\[
h(x) = \lim_{\Delta x \to 0} \left[ \frac{P(x < X < x + \Delta x | X > x)}{\Delta x} \right] \quad (4)
\]
The relationship between the hazard function and the survival function is expressed by:

\[ h(x) = \frac{f(x)}{S(x)} \]  \hspace{1cm} (5)

**Figure 1.** Survival Opportunities For Early Event and Late Event Based On Time.

### 2.4 Kaplan Meier's Survival Curve and Log Rank Test

Estimated Kaplan Meier survival function, expressed by:

\[ \hat{S}(x_{(j)}) = \hat{S}(x_{(j-1)}) \hat{P}[X > x_{(j)} | X \geq x_{(j)}] \]  \hspace{1cm} (6)

A further log rank test is used to compare Kaplan Meier's survival curves formed by the following hypothesis:

- H₀: There is no difference between the survival curves
- H₁: At least one difference between the survival curves:

Log Rank Statistic \[ = \frac{(O_i - E_i)^2}{\text{Var}(O_i - E_i)} \]  \hspace{1cm} (7)

with

\[ O_i - E_i = \sum_{j=1}^{n} (m_{ij} - e_{ij}) \]  \hspace{1cm} (8)

\( m_{ij} \) denotes the number of individuals who experience the event at time \( x_i \), and \( e_{ij} \) is the value of hope. The null hypothesis will be rejected if log rank statistics ≥ \( \chi^2_{\alpha, df} \) with degrees of freedom (df) = 1 or p-value <\( \alpha \).

### 2.5 Cox Proportional hazard model

The relationship between the hazard rate and the covariate set can be expressed using the model:

\[ \ln[h(t)] = \ln[h_0(t)] + \sum_{i=1}^{n} x_i \beta_i \]  \hspace{1cm} (9)

or \[ h(t) = h_0(t)e^{\sum_{i=1}^{n} x_i \beta_i} \]  \hspace{1cm} (10)

Where \( x_1, x_2, ..., x_n \) are covariates. \( \beta_1, \beta_2, ..., \beta_n \) are the regression coefficients to be estimated. \( t \) is time and \( h_0(t) \) is the baseline hazard rate when all covariates are zero.
2.6 Concept Framework and Research Variables

Potential independent variables affecting patient survival are tumor size, clinical stage, history of metastasis, co-morbidities, and age. Survival; the probability of breast cancer survivors to observe 3 (three) years (2013 - 2016): 1 means death (event) and 0 means life (censorship). Tumor Size; breast tumor diameter T1 (<20 cm), T2 (2 -5 cm), T3 (> 5 cm). Clinical Stage; degree or degree in breast cancer patients; consisting of 1 (Stage IV), 2 (stage IIIA, IIIB, IIC), 3 (stage I, IIA, IIB), and 4 (stage 0). History of metastasis; cancer cells that have reached to other organs with objective criteria that are present and nonexistent. Complicated disease; the presence of other diseases of breast cancer. Age; age of breast cancer patients at the beginning of treatment where 1 (60 years), 2 (41-60 years), and 3 (<40 years).

3. Results and Discussion

3.1. Kaplan Meier Analysis

The probability of survival of breast cancer patients in Ibuu Sina Hospital Makassar in 2013-2016 was indicated by unit months (0-46 months) as in table 1.

| Time (months) | Survival Rate | Tumor Size | Stadium | Metastases | Comorbidity | Age (year) |
|--------------|--------------|------------|---------|------------|-------------|------------|
| 0            | 0.861        | 0.853      | 0.835   | 0.714      | 0.674       | 0.733      |
| 5            | 0.796        | 0.784      | 0.759   | 0.565      | 0.968       | 0.667      |
| 10           | 0.741        | 0.725      | 0.696   | 0.478      | 0.567       | 0.682      |
| 15           | 0.611        | 0.588      | 0.532   | 0.348      | 0.806       | 0.690      |
| 20           | 0.491        | 0.471      | 0.418   | 0.261      | 0.661       | 0.233      |
| 25           | 0.370        | 0.343      | 0.278   | 0.217      | 0.484       | 0.436      |
| 30           | 0.293        | 0.272      | 0.199   | 0.152      | 0.399       | 0.200      |
| 35           | 0.184        | 0.164      | 0.350   | 0.024      | 0.222       | 0.212      |
| 41           | 0.086        | 0.068      | 0.050   | 0.012      | 0.113       | 0.111      |
| 46           | 0.029        | 0.023      | 0.023   | 0.023      | 0.038       | 0.037      |

Median 20 24.875 19.897 33.00 17.00 11.00 9.00 25.00 11.00 24.00 24.00 20.00 16.00

Probability of survival reached 46 months by 0.029 (2.9%). This means that if there are 100 people sufferers, then that can survive up to 46 months only 3 people only; and decreased drastically (Figure 2).
Figure 3 showed that there is a drastic decrease in survival chances of breast cancer patients who have a history of metastasis compared with patients without a history of metastasis. Meanwhile, patients with breast cancer who do not have co-morbidities are higher in survival than patients with coexisting illness (Figure 4). One of the complaints of breast cancer patients is shortness of breath caused by metastasis to the lungs causing other effects such as pleural effusion.

Figure 3. Probability of Survival of Breast Cancer Patients According to History Of Metastasis

Figure 4. Probability of Survival of Breast Cancer Patients According to Co-Morbidities.

3.2. Rank Log Test
To determine whether there are differences between the survival curve then used the log rank test.

Table 2. Rank Log Test Factors Affecting Survival of Breast

| Variable      | Log rank (Chi-Square) | df | P-value |
|---------------|-----------------------|----|---------|
| Tumor size    | 5.045                 | 1  | 0.025   |
| Clinical Stadium | 11.259                | 2  | 0.004   |
| Metastases    | 15.860                | 1  | 0.000   |
| Co-morbidity  | 11.616                | 1  | 0.001   |
| Age           | 7.763                 | 2  | 0.021   |

Based on log rank test in table 2, it can be seen that the survival of breast cancer patients based on tumor size variables, clinical stage, history of metastasis, comorbidities and age were statistically significantly different with p-value <0.05.
3.3 Cox Proportional Hazard Model

For all tumor-size factors \((x_1)\), clinical stage \((x_2)\), history of metastasis \((x_3)\), comorbidities \((x_4)\) and age \((x_5)\) allegedly affecting survival of breast cancer patients are generally modeled as:

\[
h(t) = h_0(t)e^{(\beta_1x_1 + \beta_2x_2 + \beta_3x_3 + \beta_4x_4 + \beta_5x_5)}
\]

Based on table 4 in step 1 obtained model:

\[
h(t) = h_0(t)e^{(0.87x_1 + 0.38x_2 + 0.4x_3 + 0.45x_4 + 0.50x_5 + 0.22x_6)}
\]

In step 1, the partial test shows that only PP factors are statistically significant (P-value <5%). The backward stepwise method is used to extract the least influencing factors so that the final model is obtained in step 4:

The \(\beta\) regression coefficients of the obtained models are all positive \((\beta>0)\) with the value of \(\exp(\beta)>0\), meaning that all factors included in the model influence the event speed (death). That is, the risk of failure (death) of breast cancer patients with metastasis is 1.94 times greater than that not metastases. The risk of death of breast cancer patients with comorbidities is 1.7 times greater than those that do not have co-morbidities.

| Table 3. Partial Test With Backward Stepwise Method |
|-----------------|-----------|------------|-------------|-------------|
| Variable        | \(\beta\) | Wald       | p-value     | \(\exp(\beta)\) |
|-----------------|-----------|------------|-------------|-------------|
| Step 1          | \(x_1\)   | 0.868      | 1.316       | 0.251       | 2.383       |
|                 | \(x_2\)   | 1.999      | 0.368       |             |             |
|                 | \(x_2\) (1)| 0.380      | 0.525       | 0.469       | 1.462       |
|                 | \(x_2\) (2)| 0.452      | 1.990       | 0.158       | 1.571       |
|                 | \(x_3\)   | 0.447      | 3.450       | 0.063       | 1.564       |
|                 | \(x_4\)   | 0.498      | 4.147       | 0.042       | 1.646       |
|                 | \(x_5\)   | 0.217      | 0.911       | 0.340       | 1.242       |
| Step 2          | \(x_1\)   | 1.165      | 2.605       | 0.107       | 3.207       |
|                 | \(x_3\)   | 0.588      | 6.992       | 0.008       | 1.800       |
|                 | \(x_4\)   | 0.501      | 4.174       | 0.041       | 1.650       |
|                 | \(x_5\)   | 0.213      | 0.866       | 0.352       | 1.238       |
| Step 3          | \(x_1\)   | 1.157      | 2.568       | 0.109       | 3.180       |
|                 | \(x_3\)   | 0.586      | 6.917       | 0.009       | 1.797       |
|                 | \(x_4\)   | 0.522      | 4.543       | 0.033       | 1.686       |
| Step 4          | \(x_3\)   | 0.663      | 8.941       | 0.003       | 1.941       |
|                 | \(x_4\)   | 0.535      | 4.725       | 0.030       | 1.707       |

The result of Cox PH analysis showed that the most significant and significant prognostic factor to the probability of death was the presence of metastases and co-morbidities.

4. Conclusion

The main factor causing low survival time was because the patient comes for treatment already in an advanced stage even accompanied by comorbidities (such as diabetes, anemia and hypertension). It is recommended that health workers conduct promotions to motivate women at risk for early self-examination if they know of any signs of a tumor in the breast.
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