Pressure-induced dimerization and valence bond crystal formation in the Kitaev-Heisenberg magnet $\alpha$–RuCl$_3$

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Magnetization and high-resolution x-ray diffraction measurements of the Kitaev-Heisenberg material $\alpha$–RuCl$_3$ reveal a pressure-induced crystallographic and magnetic phase transition at a hydrostatic pressure of $p \approx 0.2$ GPa. This structural transition into a triclinic phase is characterized by a very strong dimerization of the Ru-Ru bonds, accompanied by a collapse of the magnetic susceptibility. Ab initio quantum-chemistry calculations disclose a pressure-induced enhancement of the direct 4$d$-4$d$ bonding on particular Ru-Ru links, causing a sharp increase of the antiferromagnetic exchange interactions. These combined experimental and computational data show that the Kitaev spin liquid phase in $\alpha$–RuCl$_3$ strongly competes with the crystallization of spin singlets into a valence bond solid.

The Kitaev model on a honeycomb lattice has grown into a hot topic in the last decade due to its exact solubility and its quantum spin-liquid ground state, which would be relevant for, e.g., quantum computing [1, 2]. It implies a bond-dependent compass-type coupling $K$ and strong intrinsic spin frustration [3]. A crucial ingredient for realizing the Kitaev model in real materials is a strong spin-orbit coupling together with a honeycomb structure. Recently, Kitaev interactions were identified in $\alpha$–RuCl$_3$, from its unusual magnetic excitation spectrum [4, 5], its strong magnetic anisotropy [6], and electronic-structure calculations [7, 46], which renders this material an ideal platform for exploring Kitaev magnetism experimentally.

$\alpha$–RuCl$_3$ is a $j_{\text{eff}} = 1/2$ Mott insulator with a two-dimensional (2D) layered structure of edge-sharing RuCl$_6$ octahedra forming a honeycomb lattice. At ambient pressure, the honeycomb layers are arranged in a monoclinic ($C2/m$) structure at room temperature with one of the three nearest-neighbor (NN) Ru-Ru bonds slightly shorter than the other two [9]. A structural phase transition was reported at $T_N \approx 60$ K under cooling and $T_N \approx 166$ K upon warming, but the low temperature crystal structure is still under debate and could be either rhombohedral ($R3$) [10, 11] or monoclinic ($C2/m$) [12, 13]. The onset of long-range magnetic order at $T_N \approx 7$ K [9] in $\alpha$–RuCl$_3$ implies that other magnetic interactions have to be considered in addition to the Kitaev interaction $K$: a NN Heisenberg $J$, an off-diagonal coupling $\Gamma$, as well as next-NN interactions $J_2$ and $J_3$ [7, 15, 46, 51]. While electronic-structure calculations indicate that $K$ is ferromagnetic in $\alpha$–RuCl$_3$ and indeed defines the largest exchange energy scale [7, 15, 46, 51], the debate on the minimal effective spin model and precise magnitude of the different couplings is not fully settled yet. By applying a magnetic field in the basal plane, the magnetic zigzag ground state can be suppressed [6, 16, 17] and the phase above this transition was identified as a quantum spin liquid, by NMR [18], thermal conductivity [19–21], Terahertz spectroscopy [22] and neutron scattering experiments [23].

Further, it was very recently shown by specific heat, magnetization and NMR measurements [24, 25] that the Néel temperature of $\alpha$–RuCl$_3$ increases slightly with pressure and vanishes through a phase separation regime around 0.5 GPa at finite temperature. Thermal expansion measurements at ambient pressure predicted also the suppression of the magnetic order under pressure [26]. However, the initial slope value $dT_N/dp_{p=0} \approx$
−23 K/GPa from thermal expansion is in contradiction with the phase diagram drawn by the other techniques under the application of hydrostatic pressure [24, 25]. Magnetization measurements indicate a reduction of the in-plane magnetization and a high-temperature transition of unknown origin, while NMR indicates no long-range magnetic order and gapped magnetic fluctuations in the high-pressure state [25]. Furthermore, electrical resistivity studies under hydrostatic pressure exclude the possibility of a pressure-induced insulator-to-metal transition [24].

To clarify the nature of this pressure-induced phase we bring together three essential pieces of information: detailed magnetization and x-ray diffraction measurements on α-RuCl3 under hydrostatic pressure which are combined with a set of quantum chemistry electronic-structure calculations. Together they unequivocally evidence that pressure induces a first-order structural transition from the rather regular Kitaev-Heisenberg honeycomb system towards a pronounced nonmagnetic dimer state with a large difference between the long and the short Ru-Ru distance of about 0.7 Å. *Ab initio* computations for the high-pressure crystal structures reveal remarkably large isotropic antiferromagnetic couplings on the short Ru-Ru bonds, in the range of hundreds of meV, which explain the experimentally observed nonmagnetic state of α-RuCl3. We show that the \( j_{\text{eff}} = 1/2 \) picture is significantly modified under hydrostatic pressure as a result of a reduction of spin-orbit-coupling effects due to increased crystal-field splittings in the high-pressure phase.

α-RuCl3 single crystals were grown from phase-pure commercial RuCl3 powder via a high-temperature vapor transport technique [4, 21, 27]. Both magnetization and x-ray diffraction (XRD) show the homogeneous high-quality nature of our single crystals.

Magnetization under hydrostatic pressure was measured in a home-built pressure cell for a commercial superconducting quantum interference device (SQUID) magnetometer from Quantum Design. Two opposing, conical ceramic anvil pumps compress a CuBe gasket with a small hole that serves as a sample chamber [28]. Daphne oil 7373 is used as a pressure transmitting medium ensuring good hydrostatic conditions up to about 2 GPa. The pressure was applied at room temperature and determined at \( T \approx 7 \) K from the superconducting transition of a lead sample. The magnetic response for the empty cell was measured separately and subtracted from the data, in order to achieve an accuracy on the absolute value of the magnetization of about \( 2.10^{-3} \) emu/mol/Oe at \( \mu_0 H = 1 \) T.

X-ray diffraction (XRD) experiments as a function of temperature down to 30 K and pressure up to 11 GPa were performed at the beamline ID27 of the European Synchrotron Radiation Facility, using a monochromatic beam with a photon energy of 33 keV focused down to a spot size of 3x3 μm². High-quality single crystals were loaded into a membrane-driven diamond anvil cell (DAC) filled with helium as the pressure-transmitting medium. The DAC assembly was then mounted in a continuous He-flow cryostat, allowing one to cool the sample while continuously monitoring the pressure in the sample space via ruby fluorescence. Additional experiments at ID27 without a DAC, i.e. at ambient pressure, were performed as well. The collected three-dimensional data were integrated and corrected for Lorentz-, polarization and background effects using the CrysAlisPro software [29]. The subsequent weighted full-matrix least-squares refinements on \( F^2 \) were done with SHELX-2012 [30] as implemented in the WinGx 2014.1 program suite [31].

The magnetic susceptibility \( \chi \) of α-RuCl3 in the \( ab \) plane is presented in Fig. 1 as a function of \( T \) and for
different pressures up to 1.5 GPa. At ambient pressure the antiferromagnetic transition into the zigzag ordered ground state is clearly observable at $T_N \simeq 7$ K. Under a small hydrostatic pressure of 0.24 GPa, a second phase transition occurs at $T_{S2} = 140$ K with a reduction of the magnetic susceptibility below $T_{S2}$. Note that the measurement at 0.24 GPa can be interpreted as a phase separation in the sample: While a fraction of the sample is in the high-pressure state and yields a magnetization close to zero below $T_{S2}$, the second fraction still shows a paramagnetic behavior down to $T_N \simeq 7$ K, followed by an antiferromagnetic zigzag state below $T_N$. These results are qualitatively in good agreement with independent magnetization measurements [25]. While the authors in Ref. [25] measured the magnetic susceptibility on a single crystal with a single Néel temperature $T_N \simeq 13.6$ K, indicating an AB stacking of the honeycomb layers [9], the measurements reported here were performed on a single crystal with an ABC stacking as indicated by $T_N \simeq 7$ K [9]. The pressure induced collapse of the in plane magnetization in Ref. [25] with an AB stacking seems shifted to higher pressure compared to the one reported here and shows a phase separation regime on a broader pressure range up to at least $p \simeq 1$ GPa. This difference suggests that the stacking sequence would have a small influence on the structural transition $T_{S2}$.

In order to obtain a deeper insight into the pressure-induced magnetic ground state of α-RuCl₃, we performed additional measurements of $\chi$ along the transverse axis $c^*$ under hydrostatic pressure, which confirm the collapse of the magnetic susceptibility below $T_{S2}$ and thus the nonmagnetic nature of the high-pressure state of α-RuCl₃ (cf. Supplemental Material [32]).

The magnetization at 2 K as a function of the magnetic field applied in the basal plane is represented in Fig. 1(b). The magnetization at $p = 0.24$ GPa shows an upward step at $\mu_0 H_c = 4.3$ T. Since the temperature scan at 5 T represented in the inset of Fig. 1(b) confirms the absence of the antiferromagnetic transition above $H_c$, the critical field $H_c$ corresponds to the suppression of the zigzag order by an external magnetic field similar to $\mu_0 H_c \simeq 7-8$ T at ambient pressure [6, 17, 18]. Thus, the quantum critical point toward the field-induced quantum spin-liquid state seems to be strongly reduced from its ambient pressure value in this regime. At even higher pressures of 0.6 and 1.8 GPa a collapse of the magnetic signal is observed in the (pure) high-pressure state up to 5 T, preventing any extraction of the magnetic susceptibility on an absolute scale within the accuracy of our experimental setup.

The resulting temperature-pressure ($T$–$p$) phase diagram of α-RuCl₃ is given in Fig. 2. The Néel temperature stays rather constant up to about 0.2 GPa. Then, α-RuCl₃ undergoes a pressure-induced phase transition around 0.2 GPa into a nonmagnetic state with phase separation occurring over a finite pressure range. The transition temperature $T_{S2}$ increases rapidly with pressure and reaches room temperature around $p = 1.3$ GPa. This phase diagram is in good agreement with previous studies under hydrostatic pressure [24, 25] and further shows that the pressure-induced transition is of a first-order nature.

In order to elucidate the microscopic mechanisms underlying the pressure-induced transition at $T_{S2}$, we performed high-resolution XRD under hydrostatic pressure. At ambient pressure and ambient temperature our XRD measurements confirm the monoclinic $C2/m$ structure reported earlier [9, 32]. Upon increasing pressure, however, a transition $T_{S2}$ into a triclinic $P\bar{1}$ phase with Ru-Ru dimers was observed together with the changes observed in the magnetic susceptibility as shown in the phase diagram given in Fig. 2. The slight difference between the points from magnetization and from x-ray diffraction in this phase diagram can be explained by uncertainties regarding the pressure of the magnetization measurements, by finite transition widths, and by small sample dependencies [27]. The triclinic phase with Ru-Ru dimers is stable up to the highest applied pressure of 11 GPa.

In order to determine the structural changes in more detail, we performed refinements of the measured intensities at various pressures. The obtained structural changes upon entering the triclinic high-pressure phase are illustrated in Fig. 3. Besides changes in the relative...
FIG. 3. Honeycomb layer of the α-RuCl₃ structure at 300 K in the monoclinic phase at ambient pressure (left) and in the triclinic phase at 2.08 GPa (right). The ellipses represent the pressure-induced Ru-Ru dimers.

FIG. 4. Bonding (top) and antibonding (bottom) combinations of the Ru₄t₂g hole orbitals on the shorter Ru-Ru bonds of the crystal structure in the dimer state, as obtained by embedded-cluster quantum chemistry calculations.

positions of neighboring Ru₃Cl₃-layers, there are dramatic changes within the layers themselves. At ambient pressure (left panel of Fig. 3), the differences in the Ru-Ru distances are only about 0.003 Å (Table 1 of Supplementary Material [32]), resulting in a nearly hexagonal honeycomb lattice. The transformation into the triclinic phase with increasing pressure involves the formation of Ru-Ru dimers with a large difference between the short and the long Ru-Ru distances of about 0.7 Å. This extremely strong dimerization involves all Ru atoms, i.e., every Ru atom is part of a dimer.

To clarify the effect of this dimerization on magnetism, we carried out embedded-cluster quantum-chemistry calculations using the experimental crystal structures. Our \textit{ab initio} results show that in the triclinic phase the 4d-shell t₂g crystal-field splittings are very large, up to 0.35 eV, and counteract the effect of spin-orbit coupling. The $j_{\text{eff}}=1/2$ picture is therefore significantly modified and given the peculiar character of the Ru t₂g hole, an antiferromagnetic isotropic spin model turns out to be a rather good approximation on the shortest Ru-Ru links, with an impressively strong antiferromagnetic exchange. Specifically, we find that two of the 4d t₂g levels are nearly degenerate, lie at lower energy (electron picture), and that the t₂g hole is mainly associated with the high-energy orbital that provides a large direct d-d overlap on the shortest Ru-Ru bonds, as sketched in Fig. 4. By multireference configuration-interaction (MRCI) calculations [50] we derive singlet-triplet separation energies as high as 440 and 550 meV for the shortest Ru-Ru links found experimentally at 300 K for 4.6 and 10.6 GPa, respectively, with vanishing splittings among the triplet components. So large energy differences between the singlet and triplet states associated with two NN t₂g ions imply that a finite magnetization can only be achieved by very large magnetic fields, which is indeed observed in Fig. 1(b), and also explain the large spin-excitation gap observed in a recent NMR study of α-RuCl₃ under pressure [25].

For the longer Ru-Ru links, the relevant effective model is an extended pseudospin-1/2 Hamiltonian with both

\begin{table}[h]
\begin{center}
\caption{NN magnetic couplings (meV) for high-pressure crystal structures as determined at room temperature; results of spin-orbit MRCI calculations for the longer Ru-Ru links, where the isotropic and anisotropic components still have comparable strength.}
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Pressure (GPa) & $K$ & $J$ & $\Gamma_{xy}$ & $\Gamma_{xz}$ & $\Gamma_{yz} = -\Gamma_{yz}$ \\
\hline
4.60 & -3.15 & 3.32 & -0.22 & -0.95 \\
10.60 & -1.75 & 0.81 & 0.80 & -0.49 \\
\hline
\end{tabular}
\end{center}
\end{table}
isotropic and anisotropic components \cite{46},
\begin{equation}
\mathcal{H}_{i,j} = J \mathbf{S}_i \cdot \mathbf{S}_j + K \mathbf{S}_i^z \mathbf{S}_j^z + \sum_{\alpha \neq \beta} \Gamma_{\alpha\beta}(\mathbf{S}_i^\alpha \mathbf{S}_j^\beta + \mathbf{S}_j^\beta \mathbf{S}_i^\alpha),
\end{equation}

where $\mathbf{S}_i$ and $\mathbf{S}_j$ are NN pseudospin 1/2 operators and the $\Gamma_{\alpha\beta}$ coefficients stand for off-diagonal couplings of the anisotropic exchange tensor with $\alpha, \beta \in \{x, y, z\}$. Mapping the spin-orbit MRCI results onto such an effective model \cite{46, 47}, we arrive at the NN couplings listed in Table I for the long links of the dimerized structure at 4.6 GPa and 10.6 GPa.

The combined experimental and theoretical results therefore reveal a competition between spin-orbit coupling and covalency effects. Interestingly, a second crystal structure, $\beta$-RuCl$_3$, with Ru chains at room temperature and Ru dimers at low temperature was reported \cite{35}. Previous density-functional calculations predicted that $\alpha$-RuCl$_3$ would also dimerize in the absence of spin-orbit coupling \cite{36}. While at ambient pressure the spin-orbit coupling is significantly larger than the crystal-field splittings to stabilize a Ru $j_{\text{eff}} \simeq 1/2$ state, with increasing pressure a phase dominated by strong covalency appears \cite{37–39}. This mechanism may also apply to other 4$d$ and 5$d$ metal halides and oxides such as $\alpha$-MoCl$_3$ at ambient pressure \cite{40, 41} and the Kitaev-Heisenberg iridate $\alpha$-Li$_2$IrO$_3$ at a critical pressure $p_c \simeq 3.8$ GPa \cite{42}. Thus dimerization may be a rather general feature of 4$d$ and 5$d$ honeycomb systems, due to a subtle interplay between spin-orbit coupling, intermetallic bonding, and magnetism.

In summary, our magnetization and x-ray diffraction experiments on $\alpha$-RuCl$_3$ under hydrostatic pressure show a pressure-induced phase transition from the monoclinic to a triclinic structure, featuring a very pronounced Ru-Ru dimerization and a valence bond crystal of ordered dimers. The latter are characterized by remarkably strong antiferromagnetic isotropic couplings due to an increased direct overlap of the Ru 4$d$ $t_{2g}$ orbitals. This dimerization leads to a complete suppression of the magnetization and thus to a pressure-induced nonmagnetic state of $\alpha$-RuCl$_3$. Our results show that the Kitaev physics in this d-electron honeycomb system is in competition with the formation of spin singlet valence bonds: Indeed, $\alpha$-RuCl$_3$ shows the occurrence of both a quantum spin liquid state under magnetic field, which is relevant for its topological properties, and a spin solid under hydrostatic pressure: the spin singlet valence bond crystal. Thus, this material will provide new insights for the study of concomitant magnetic and lattice instabilities in 4$d$ and 5$d$ metal halides and oxides.

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