Computational Fluid Dynamics Model of Wells Turbine for Oscillating Water Column System: A Review

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Abstract. Wells turbine is an important component in the oscillating water column (OWC) system. Thus, many researchers tend to improve the performance via experiment or computational fluid dynamics (CFD) simulation, which is cheaper. As the CFD method becomes more popular, the lack of evidence to support the parameters used during the CFD simulation becomes a big issue. This paper aims to review the CFD models applied to the Wells turbine for the OWC system. Journal papers from the past ten years were summarized in brief critique. As a summary, the FLUENT and CFX software are mostly used to simulate the Wells turbine flow problems while SST k-ω turbulence model is the widely used model. A grid independence test is essential when doing CFD simulation. In conclusion, this review paper can show the research gap for CFD simulation and can reduce the time in selecting suitable parameters when involving simulation in the Wells turbine.

1. Introduction
Ocean energy is among the primary sources of renewable energy other than Solar, Wind, Hydroelectric, Biomass, Geothermal [1]. Under ocean energy, wave energy is considered energy with a high potential as a renewable energy, but it is mainly untapped [2]. The main benefit of wave energy is having high energy density [3], high source availability [4], high load factor [3], source predictability compared to other renewable energy sources [3] and environmentally friendly [3–5]. A machine that absorbs wave energy and converts it into useful energy is called a wave energy converter (WEC).

The oscillating water column (OWC) is a wave energy converter (WEC) system with a simple working principle but has good efficiency. When the wave is at the crest, water will go into the water chamber and increase the water column. This water column will push and compress the air in the air chamber. The compressed air located in the air chamber then will push the blade at the air turbine, thus generating power. This is called exhalation process. Meanwhile, for the inhalation process, as the wave is at a trough, the water column will decrease, and the air will expand again. Even though the air is expanded, there will be no reverse rotation of the blade turbine, as it was designed to move only in one direction. This cycle is repeated continuously as wave crest and trough and will generate power. There are several types of turbines used in this OWC system.

The air turbine is the heart of the OWC system. Wells and Impulse turbines are the most common turbines used to compare to the cross-flow, Savonius [6], Hanna [7], or even Denniss-Auld [8] types. Although the operational flow range of the impulse turbine is wider than the Wells turbine, its peak efficiency hardly exceeds about 50 %, the main reason why the study focused more on the Wells turbine [8].

The early development of the Wells turbine created by Arthur Alan Wells in 1976 was based on the researchers’ experiments, which was considered time and cost-consuming. Thus, in brief, this paper
summarises that the time taken to select appropriate parameters in doing future CFD simulations can be reduced.

2. Wells Turbine

Wave energy converter can be divided into several types as shown in Figure 1. Includes fixed structure, floating, submerged, and floating structure with concentration i.e. wave dragon. All these types of WECs described have the unique advantage of producing the same function and purpose. Figure 2 shows the typical arrangement of the OWC system with the working principle of the system [6]. Inside the air chamber contains a very important device in a WEC which is a turbine. The Wells turbine as shown in Figure 3(a) was placed at the hub which is connected to a shaft. This shaft is responsible for rotating the generator to generate the power output. The Wells turbine was placed in an enclosure casing. The turbine can only rotate in one direction regardless of the air oscillating flow direction. This is due to the symmetrical blade profile used in the Wells turbine. The symmetrical blade profile usually belongs to the NACA 00XX series.

Several types of Wells turbines were investigated by the researchers [8], [11]–[14]. The simplest is the single-plane Wells turbine as shown in Figure 3(a). This type of turbine just has one set of Wells turbines on one plane. The other type of Wells turbine is a biplane Wells turbine, which means that the turbine is arranged in two planes. Wells turbine with guide vanes is another type of Wells turbine as shown in Figure 3(b). The guide vanes can be placed for single plane and biplane Wells turbine. As for the biplane Wells turbine, the guide vanes can be placed in the outer or intermediate direction of the turbine. The biplane with both turbines moving in different directions is called a contra-rotating Wells turbine. The least concerned Wells turbine is the self-pitching Wells turbine, which means that the
turbine does not have a fixed pitch angle, but the angle is set free to follow the direction of the oscillating flow. The fundamental theory for each of these types was mentioned briefly by Falcão and Gato [11].

![Figure 3. (a) Standard single plane Wells turbine [15] and (b) single plane Wells turbine with guide vanes [16]](image)

Optimizing the Wells turbine is focused on the blade of the Wells turbine. There are eight important parameters in optimizing the Wells turbine which are the blade profile (thickness ratio), blade solidity, blade pitch angle, blade end plate, blade aspect ratio, blade sweep, blade tip clearance and blade tip ratio [17]. According to Das, Halder, and Samad, blade solidity and tip clearance are the most important parameters among the many parameters that influence the performance of the Wells turbine [6].

The main concern of optimizing the Wells turbine is to maximize the performance of the turbine. Power output, flow rate, operational range, efficiency and pressure drop are the main parameters used as an indicator for Wells turbine performance [17]. These factors relate to each other. Thus, the most important parameter should be focused on when designing and optimizing the Wells turbine. In most cases, having a wide operating range is preferable compared to the efficiency of the turbine [6].

3. Methodology

Journals on CFD simulation on the air and hydraulic Wells turbine in the past ten years have been selected. Theses and reports were not considered in the selection. From the selected journals, the turbulence model used with the corresponding Reynolds number together with the number of elements used during the simulation are tabulated in Table 1. The mesh and type of topology used during the simulation were placed at the last column of Table 1.

4. Discussion

Before running CFD simulation in the software, important settings should be incorporated into the software. These settings are important and essential to obtain accurate and correct results. Table 1 shows the settings used in the simulation by the researchers. The table consists of the year with reference, the turbulence model used in their CFD simulation, Reynolds number obtained for the simulation, number of elements, and mesh or topology used in the simulation. A brief review on each of the setting is mentioned in the next sub-section.

| Year [Ref] | Turbulence Model | Reynolds Number | No of Elements | Mesh / Topology |
|------------|------------------|-----------------|----------------|-----------------|
| 2010 [18]  | R k–ε            | $0.74 \times 10^5, 4.41 \times 10^5$ | 295,500        | ST, HX, OG      |
| 2011 [19]  | R k–ε            | $0.68 \times 10^5, 4.41 \times 10^5$ | 295,500        | ST, HX, OG      |
| 2011 [20]  | R k–ε            | 2.4 x 10^5      | 2,120          | NA              |
|            |                  |                 | 60,000*        |                 |
|            |                  |                 | 80,000*        |                 |
|            |                  |                 | 119,000        |                 |
| 2011 [21]  | SST k-ω          | NA              | 4,000,000      | ST, HX, MB      |
| Year [Ref] | Turbulence Model       | Reynolds Number | No of Elements          | Mesh / Topology       |
|------------|------------------------|-----------------|-------------------------|-----------------------|
| 2012 [22]  | R k–ε                 | NA              | 735,540                 | ST, HX, OG, HG        |
|            |                        |                 | 834,000                 |                       |
|            |                        |                 | 933,000                 |                       |
|            |                        |                 | 1,032,000               |                       |
|            |                        |                 | 1,131,540               |                       |
| 2012 [23]  | R k–ε                 | NA              | 1,236,576               | ST                    |
|            |                        |                 | 1,534,016               |                       |
| 2012 [24]  | R k–ε*, RNG k–ε, SST k-ω | NA         | 424,686                 | ST, HX                |
| 2013 [25]  | R k–ε                | NA              | 1,194,320               | ST, HX                |
| 2014 [26]  | SST k-ω              | 5 x 10^5        | 1,800,000               | ST, OG                |
| 2014 [27]  | R k–ε                | 2.4 x 10^5      | 2,120                   | NA                    |
|            |                        |                 | 60,000*                 |                       |
|            |                        |                 | 80,000*                 |                       |
|            |                        |                 | 119,000                 |                       |
| 2014 [28]  | SST k-ω              | 4.5 x 10^5      | 1,800,000               | ST, OG                |
| 2014 [29]  | R k–ε*, SST k-ω, S-A  | 6 x 10^5 - 2 x 10^5 | 312,951                 | ST                    |
| 2014 [30]  | SST k-ω              | NA              | 1,425,044               | ST, HX                |
| 2015 [31]  | SST k-ω              | NA              | 1,368,000               | ST, HX, MB            |
| 2015 [32]  | SST k-ω              | NA              | 764,416                 | ST, HX                |
|            |                        |                 | 1,424,016*              |                       |
|            |                        |                 | 1,589,250               |                       |
|            |                        |                 | 1,784,000               |                       |
| 2016 [33]  | k–ε, R k–ε*, SST k-ω, R k–ε* | 2.9 x 10^5 | 410,000                 | HM                    |
|            |                        |                 | 500,000*                |                       |
|            |                        |                 | 530,000                 |                       |
| 2016 [34]  | SST k-ω              | 1.3 x 10^5 - 3.1 x 10^5 | 1,000,000               | ST, CG, HG, MB        |
| 2016 [35]  | k–ε, S-A             | 2.2 x 10^5      | 3,000,000               | PD                    |
| 2016 [36]  | SST k-ω              | 4 x 10^5, 8 x 10^5 | 1,300,000               | ST, HX                |
| 2017 [37]  | SST k-ω              | NA              | 1,200,000               | UT                    |
|            |                        |                 | 1,600,000               |                       |
|            |                        |                 | 2,000,000               |                       |
|            |                        |                 | 5,400,000               |                       |
| 2017 [38]  | k–ε, S-A, SST k-ω, γ-Reθ* | 0.8x10^5, 1.5x10^5 | 1,000,000               | ST, CG, HG, MB        |
| 2017 [39]  | k–ε, SST k-ω*        | 5.2x10^5        | 1,200,000               | UT                    |
|            |                        |                 | 1,600,000               |                       |
|            |                        |                 | 2,100,000               |                       |
| 2017 [40]  | SST k-ω              | 5.2x10^5        | 400,000                 | UT                    |
|            |                        |                 | 600,000*                |                       |
|            |                        |                 | 800,000                 |                       |
| 2017 [41]  | R k–ε               | NA              | 2,580,800               | UT, TX                |
| 2017 [42]  | S-A                | NA              | 1,964,000               | ST, CG, HG, MB        |
| 2017 [43]  | SST k-ω              | 1.3x10^5, 3.1x10^5 | 1,000,000               | ST, CG, HG, MB        |
| 2017 [44]  | R k–ε               | NA              | 266,756                 | ST, OG, HG            |
|            |                        |                 | 990,204                 |                       |
|            |                        |                 | 1,571,704*              |                       |
|            |                        |                 | 1,755,876               |                       |
| 2017 [45]  | R k–ε               | NA              | 799,594                 | ST, OG, HG            |
|            |                        |                 | 941,732                 |                       |
|            |                        |                 | 1,114,358               |                       |
|            |                        |                 | 1,307,852               |                       |
|            |                        |                 | 1,550,154*              |                       |
| 2018 [46]  | SST k-ω              | 1 x 10^5        | 24,500                  | CG, HG                |
|            |                        |                 | 35,000                  |                       |
|            |                        |                 | 45,500                  |                       |
|            |                        |                 | 700,000                 |                       |
|            |                        |                 | 1,000,000               |                       |
| Year | Turbulence Model | Mesh | Topology | Note |
|------|-----------------|------|----------|------|
| 2018 [47] | R k-ε | NA | UT, HX | |
| 2018 [48] | R k-ε | NA | UT, TX | |
| 2018 [49] | SST k-ω | 5.33 x 10^5 | ST, MB | |
| 2018 [50] | SST k-ω | NA | ST, CG, MB | |
| 2018 [51] | S-A | NA | UT | |
| 2018 [52] | SST k-ω | NA | ST | |
| 2018 [53] | SST k-ω | 2 x 10^5 | ST, HG, CG, MB | |
| 2018 [54] | SST k-ω | NA | UT, TX | |
| 2018 [55] | SST k-ω | NA | UT | |
| 2019 [56] | SST k-ω | NA | UT | |
| 2019 [57] | SST k-ω | NA | UT, TX | |
| 2019 [58] | SST k-ω | 6.5 x 10^5 - 6.6 x 10^5 | UT | |
| 2020 [59] | SST k-ω | 5.25 x 10^5 - 5.43 x 10^5 | UT | |

Turbulence Model: Standard k-ε (k-ε), Realizable k-ε (R k-ε), Shear stress transport k-ω (SST k-ω), Renormalization Group k-ε (RNG k-ε), Spalart-Allmaras (S-A), Menter transitional model (γ-Reθ). Mesh: Unstructured (UT), Structured (ST), Hybrid-Mesh (HM), Hexahedral (HX), Tetrahedral (TX), Polyhedral (PD). Topology: O-Grid (OG), H-Grid (HG), C-Grid (CG), Multi-Block (MB). NA – Not Available. # - nonstandard wall function, * - used in the final simulation.

4.1 Turbulence model

Selecting the suitable turbulence model for simulation is important. An unsuitable turbulence model may lead to overprediction or underprediction of the results. Based on Table 1, 15 papers used R k-ε as the turbulence model corresponding to 36%, while about 23 papers (55%) used SST k-ω, three papers used the S-A model and one paper used γ-Reθ.

Using previous data from other researchers, Mohamed et al. [6] used R k-ε. The previous researcher compared k-ε, RNG k-ε, R k-ε, SST k-ω and RSM with experimental data. Čarija et al. [24] suggested that the R k-ε model is the best fit for experimental work compared to RNG k-ε and SST k-ω models. While Shehata et al. [29] concluded that R k-ε is the best model compared to SST k-ω and S-A; however,
the results between R $k-\varepsilon$ and SST $k-\omega$ is similar, and R $k-\varepsilon$ uses less computing time compared to SST $k-\omega$. In this simulation, grid-independent test was not done. Cui and Hyun [33] also concluded that R $k-\varepsilon$ is the best model compared to $k-\varepsilon$, SST $k-\omega$ and R $k-\varepsilon$ with nonstandard wall function and SST $k-\omega$ giving the highest deviation from the experimental results. The author mentioned the grid-independent test, but the outcome of the simulation was not mentioned in detail.

In contrast, Ghisu et al. [34] mentioned that SST $k-\omega$ was chosen as the turbulence model based on the previous simulation) compared with several models. The researcher will use the same model for their future works [53]. Ghisu, Puddu, and Cambuli [38] suggested that $\gamma$-$Re_0$ is the best model compared to $k-\varepsilon$, S-A, and SST $k-\omega$. They stated that this is because the Reynolds number for the simulation is under transition period and not in turbulence period.

Hu, Li, and Wei [35] compared between S-A and $k-\varepsilon$ model. They concluded that the S-A model predicts better than the $k-\varepsilon$ model. But it should be known that grid independence was not done in this study. Later they used this model for another research [51]. Mahboubidoust and Ramiar [42] also used S-A as the turbulence model by using the findings by Torresi et al. [60].

Most of the early simulation studies that used SST $k-\omega$ as the turbulence model stated that this model is widely used in turbomachine CFD simulations [26], [28], [30], [61], [62]. Gratton et al. [46] used the findings by Torresi et al. [63] to use SST $k-\omega$ as the turbulence model, while Nazeryan and Lakzian [49] found that simulation using SST $k-\omega$ as the turbulence model is in good agreement with the experimental data. This finding is the same with Halder, Samad, and Thévenin [39]. Das and Samad [58], [59] using SST $k-\omega$ based on research by Douvi [64] stated that this turbulence model is suitable for NACA aerofoil simulation.

In conclusion, SST $k-\omega$ is the best turbulence model for use in the Wells turbine CFD simulation, which was supported by Douvi’s [51] research on NACA aerofoil and comparison data from simulation and experiment [39], [49]. S-A turbulence model is also in good agreement with simulation and experimental data. However, this model fails to predict stall point [65]. Another good model that can be used is R $k-\varepsilon$. This model also produces results in line with the experimental results. It should be considered that the flow of the model should exceed the critical Reynolds number so that the model can predict the result precisely [38].

4.2 Reynolds Number

Calculating Reynolds number is very crucial in CFD simulations. Knowing Reynolds number can differentiate the flow whether it is laminar, transition, or turbulent flow. Takao et al. stated that the critical Reynolds number is $4 \times 10^5$ [66]. Thus, a simulation with a Reynolds number bigger than $4 \times 10^5$ is suitable for the turbulence model. Table 1 shows that some of the researchers did not mention the value of the Reynolds number in their simulations.

Meanwhile, some researchers have flow in transition mode, but they used the turbulence model in their simulation, which may be why some of the turbulence model results differ between researchers. Ghisu et al. [38] also stated this in their research that had transition flow, and their transition model fit well with the results compared to the turbulence models. To differentiate the flow between transition and turbulence, the critical Reynolds number should be compared. But, up-to-date, only Takao et al. stated the value of critical Reynolds number [66] as $4 \times 10^5$. As Reynolds numbers is an important factor in CFD simulation, the critical Reynolds number in simulating Wells turbine is considered as one of the research gaps as no other research was done after Takao et al. [66] in 2006. This parameter is important as the newly suggested value of the critical Reynolds number can be lower or even higher than the value suggested by Takao et al. [66], which can lead to different output.

4.3 Grid Independence test

Another important test when dealing with CFD simulation is the grid independence test. This test is done to minimize the influence of grid size on the CFD simulation results [67]. As shown in Table 1, few researchers did not run the grid independence test in their research, giving some degree of ambiguity in their CFD simulation results. In the past few years, most of the researchers included the test in their
simulation. There are also some researchers [50] that included this test in their research but did not document it properly. Even though this test is important, there is still no a standardized test method or procedure to run the test [68]. Three common methods used in this test are the grid resolution method, general Richardson extrapolation method and grid convergence index [69]. In the reviewed paper, most of the tests used were based on the grid resolution method and only Das and Samad [58] used the grid convergence index method.

4.4 Meshing and topology
As for meshing, no researcher mentioned any advantages between the structured and unstructured or otherwise, as the meshing can be used according to suitability. It should be noted that despite the unstructured mesh being able to handle complex geometries, it requires higher computational time compared to structured mesh [70]. In general, structured mesh can be considered as sufficient to handle Wells turbine blade CFD simulation. Hybrid meshing can be used to compromise the advantages and disadvantages of structured and unstructured meshing.

It is common to use structured meshing with Hexahedral and unstructured meshing with Tetrahedral. Polyhedral meshing is the least concern meshing type. Only researcher that using Star-CCM+ used this meshing. No specific advantages are known in using this meshing. As for topology, in some complex geometry or to tackle critical parts of the simulation, the multi-block should be used together with O-Grid, H-Grid, or C-Grid. This can increase the result accuracy of the main concerning region.

5. Conclusion
In summary, 42 journal papers related to CFD simulation on Wells turbine were briefly summarised. FLUENT and CFX software were recommended to be used to simulate the Wells turbine flow problem with SST k-ω turbulence model. In order to avoid discrepancies in that result, Reynolds number of the flow should be higher than the critical Reynolds number, 4 x 10^5. Grid independence test is a must to reduce the error in the result. There is no specific recommendation for meshing and topology, as there is no significant improvement between structured and unstructured meshing. However, the capability of the computer should be considered when dealing with unstructured mesh.

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