Phase-Only Space-Time Adaptive Processing

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ABSTRACT Space-time adaptive processing (STAP) is a well-known and effective method to detect targets, obscured by interference, from airborne radars that works by coherently combining signals from a phased antenna array (spatial domain) with multiple radar pulses (temporal domain). As widely demonstrated, optimum STAP, in the sense of maximizing the output signal to interference plus noise ratio (SINR), is a coherent, linear, transversal filter (i.e., tapped delay line), that can be synthesized by a complex-valued weight vector. This paper extends previous work that focused on adaptive spatial-only nulling; it derives the optimum phase-only STAP, namely, the optimal weight vector that maximizes the SINR subject to the constraint it belongs to the $N$-torus of phase-only complex vectors, where $N$ is the number of spatio-temporal degrees of freedom. Because this problem does not admit a closed-form solution, it is solved numerically using the phase-only conjugate gradient method (CGM). The effectiveness of phase-only STAP is demonstrated using both SINR values and receiving beampattern shape, comparing it with the optimum fully-adapted STAP and the nonadapted beam former responses as well as other possible counterparts. Additionally, several analyses of practical utility also demonstrate the benefits provided by phase-only STAP.

INDEX TERMS Radar signal processing, space time adaptive processing (STAP), adaptive radar receiver, phase-only adaptive nulling, phase-only STAP, gradient descent method.

I. INTRODUCTION

Radar space-time adaptive processing (STAP) is a powerful technique used in airborne systems to detect a target embedded in interference potentially comprising clutter, jamming and noise [1]–[5]. More in details, STAP is the processor capable of jointly combining the signals acquired by multiple antenna’s elements of a phased-array, indicated as the spatial or angular domain, and in a coherent processing interval (CPI) composed by multiple pulse repetition intervals (PRIs), that is the temporal or Doppler domain [2]. By doing so, even if the target is indistinguishable in a single space or time domain, it would be visible (and hence detected, tracked and classified) in the joint space-time domain [2], [4]. It is worth highlighting that STAP can be seen as a two-dimensional (2-D) filter jointly combining beamforming and Doppler filtering [2]. In particular, it should be observed first that in analyzing the detection capabilities of a radar system it is essential to take into account the signal to interference plus noise ratio (SINR) that provides a measure of the radar strength to distinguish the target component with respect to the interferences in the received signal. Therefore, assuming a radar transmitting a coherent pulse train through a phased-array antennas, it should be proved (see [6] for more details) that the processor that maximizes the output SINR is a coherent, linear, transversal filter.

Due to the primary role of this processing in airborne radars, exhaustive technical literature has been published on this interesting and challenging topic aimed at improving several characterizing aspects [9]. Methodologies for the on-line computation of the weight vectors in STAP have been proposed and some applied in practice in [10]–[14]. These methods exploit computationally efficient techniques as well as lattice-based algorithms to obtain a variety of adapted beam focused on different directions and Doppler frequencies and, at the same time, strongly reducing the computational burden.

1STAP finds application to also other contexts such as to synthetic aperture radar (SAR) processing [7], [8].
burden towards real-time implementations. Moreover, several studies have been conducted to demonstrate the effectiveness of the radar STAP in such environments that go beyond the classic homogeneous assumption [15]–[19]. For instance, in [18], space-time models for both amplitude and spectral clutter heterogeneity are proposed and the losses experienced by STAP have been evaluated under these circumstances. Then, in [20] optimal and adaptive reduced-rank (both two- and three-dimensional) STAP algorithms for joint hot and cold clutter mitigation are provided. Analogously, also in [21] some applications of reduced-rank methods for STAP have been described and deeply analyzed. Again, some works, e.g. [22]–[25], have investigated the potential exploitation of some a-priori information about the disturbance covariance to improve the radar STAP detection capabilities. Moreover, in [26] a partially adaptive STAP based on the so-called FRACTA (a reiterative censoring and detection procedure) algorithm is implemented aiming at reducing the computational complexity as well as the required sample support. Other developments have been provided in [27], where the authors propose a code design algorithm based on the maximization of the detection performance of a radar STAP controlling the regions of achievable values for the temporal and spatial Doppler estimation accuracy, as well as the degree of similarity with a pre-fixed radar code. Moreover, [28] models the disturbance as a low-rank spherically invariant random vector (SIRV) clutter plus a zero-mean white Gaussian noise and proposes a STAP algorithm framed within this context exploiting the projection of the estimate in the clutter subspace. In [29], a robust adaptive beamforming is developed in the presence of some mismatches in the desired signal and the disturbance covariance for a factored radar STAP. Beyond STAP, some interesting developments can be found in [30]–[34], where a joint design of transmit waveform and receive filter is performed using the output SINR as objective function.

All the above-mentioned research papers are essentially based on the computation of the weight vector, that for the optimum adapted radar STAP (i.e., that maximizing the SINR) is essentially described by a number of complex quantities that would be multiplied to the received signal samples in the receiving filter. However, in several practical implementations, the radar receiver could comprise only phase shifters not-always sharing also amplitude tuners; therefore, it would be interesting to implement complex weights having a constant modulus, namely to derive a phase-only weight vector. This problem has been addressed in [35], where the optimum phase-only adaptive array has been designed formalizing the problem as a SINR maximization constraining the weight vectors to belong to the phase-only space. The problem has been solved thanks to two different algorithms that are the phase-only conjugate gradient method (CGM) and the Newton’s method. This paper addresses the problem of optimum phase-only STAP, extending the work focused on phase-only adaptive spatial nulling of [35] filling the gap towards the radar STAP. The idea is to find the STAP weight vector maximizing the SINR constraining it to belong to the space of phase-only vectors. As in [35], also in this case the problem does not admit a closed-form solution, and it is solved resorting to the phase-only CGM. Even if the considered method provides only a local maximization of the SINR, a proper selection of the starting point allows to reach near-optimum performance. The effectiveness of the phase-only STAP is shown in the analysis section, evaluating the receiving beampattern shape, the achievable SINR, and the sidelobes level of the adapted two-dimensional beam also in comparison with the optimum adapted STAP as well as to other possible counterparts. An analysis of the phase behavior, also in the presence of a limited number of bits to code them, is performed to highlight the effectiveness of this method also in practical situations. Additionally, the fully-adapted phase-only STAP architecture is analyzed to verify the validity of the Reed-Mallet-Brennan rule [36]. Finally, a method for jointly optimizing the transmitted waveform and the receiving filter, constraining both of them to be phase-only vectors, is also provided.

Summarizing, the main contributions of this paper are:

- the derivation of the optimum phase-only STAP extending a previous work that focused on adaptive spatial-only nulling;
- extensive analyses of the phase-only STAP in several interfering scenarios of interest and to practical implementations;
- the application of the method for jointly optimizing the transmitted waveform and the receiving filter, constraining both of them to be phase-only vectors.

The paper is organized as follows. Section II briefly recalls the STAP concept, introduces the formalism together with the description of the considered radar architecture. Then, Section III presents the phase-only STAP and provides the description of the used solution based on the CGM. The performance analyses are conducted and discussed in Section IV. Conclusions and suggestions for possible future developments are given in Section V.

Notation:

We use boldface for vectors $\mathbf{a}$ (lower case) and matrices $\mathbf{A}$ (upper case). The transpose and the conjugate transpose operators are denoted by the symbols $(\cdot)^T$ and $(\cdot)^*$ respectively. $\text{Diag}(\mathbf{a})$ is the diagonal matrix whose $i$-th diagonal element is the $i$-th entry of $\mathbf{a}$, whereas $\text{Diag}(\mathbf{A})$ is the diagonal part of the matrix $\mathbf{A}$. $\mathbf{I}$ refers to the identity matrix (its size is determined from the context). $\mathbb{C}^{N}$ and $\mathbb{T}^{N}$ are the sets of $N$-dimensional vectors of complex numbers and elements of the phase-only torus, respectively. The symbols $\otimes$ and $\odot$ indicate the Kronecker and the element-wise or Hadamard product, respectively. The letter $j$ represents the imaginary unit (i.e. $j = \sqrt{-1}$). For any complex number $x$, $|x|$ indicates its modulus, and $\text{Im}(x)$ indicates its imaginary part. The Frobenius matrix norm is denoted by $\| \cdot \|$, and $\mathbb{E} [\cdot]$ is statistical expectation. Finally, $[\mathbf{A}, \mathbf{B}]$ between matrices $\mathbf{A}$ and $\mathbf{B}$ is the Lie bracket or commutator product defined as $\mathbf{A} \mathbf{B} - \mathbf{B} \mathbf{A}$. 

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II. OPTIMUM SPACE-TIME ADAPTIVE PROCESSING

This section formalizes the concept of space-time adaptive processing together with the description of the respective optimum radar receive filter. To do this a pulse-Doppler radar comprising \( L \) spatial channels and transmitting \( M \) coherent pulses is taken into account. Hence, the radar antenna is a uniformly spaced linear array antenna (ULA) consisting of \( L \) elements. Indicating with \( \theta \) the azimuth angle variable, the spatial steering is given by

\[
v_s(\theta) = \begin{bmatrix} e^{j\phi_1 \sin(\theta)}, \ldots, e^{j\phi_{L-1} \sin(\theta)} \end{bmatrix}^T,
\]

having implicitly assumed that the space between antenna’s elements is equal to \( d = \lambda_0/2 \), with \( \lambda_0 \) the radar operating wavelength. The radar is assumed to transmit a coherent train of \( M \) pulses at regular pulse repetition interval (PRI), say \( T \). Therefore, indicating with \( v_P \) the frequency variable representing the Doppler frequency normalized to \( \text{PRF} = 1/T \), the temporal steering is

\[
v_t(v_P) = \begin{bmatrix} 1, e^{j2\pi v_P}, \ldots, e^{j2\pi (M-1)v_P} \end{bmatrix}^T.
\]

Then, the joint spatio-temporal steering vector of size \( N = ML \) is defined to be

\[
v(v_{DP}, \theta) = v_t(v_P) \otimes v_s(\theta).
\]

For sake of brevity, in what follows, the dependence of \( v \) on \( v_{DP} \) and \( \theta \) will be omitted. Let us now denote by

\[
\mathbf{r} = \mathbf{v} + \mathbf{n}
\]

the \( N \)-dimensional vector associated to the received signal of the cell under test, where \( \mathbf{n} \) is the zero-mean vector associated to the disturbance components. Then, it can be demonstrated that the optimum filter output is given by the inner product between the weight vector and the useful signal, namely

\[
\mathbf{s} = \mathbf{w}^\dagger \mathbf{r},
\]

where \( \mathbf{w} \in \mathbb{C}^N \) is the complex \( N \)-dimensional weight vector.

Moreover, denoting by \( \mathbb{E}[\mathbf{nn}^\dagger] = \mathbf{M} \) the unknown disturbance (viz. clutter plus directional interference plus noise) covariance matrix, the SINR at the output of the above mentioned filter is

\[
\text{SINR} = \frac{\|\mathbf{w}^\dagger \mathbf{v}\|^2}{\mathbf{w}^\dagger \mathbf{M} \mathbf{w}}
\]

It can be shown that the SINR described in (6) attains its maximum when the weight vector is chosen as

\[
\mathbf{w} = \mathbf{M}^{-1} \mathbf{v},
\]

that is typically referred to as the optimum radar receiver filter [2], [3] whose schematic representation is given in Figure 1. As it can be clearly observed from (7), the optimum receiving filter for STAP essentially assumes the knowledge of the steering vector \( \mathbf{v} \) and requires the computation of the disturbance covariance matrix. Conversely, a phase-only adaptive radar STAP is based on the computation of the complex weights that are described by only a phase term and that maximizes the SINR in (6). A direct method to estimate the optimum phase-only weight vector does not exist and requires the use of gradient-based methods. In the next section, following the same line of reasoning of [35], an effective method based on the Hestenes and Stiefel’s conjugate gradient algorithm [37] is derived.

![Block scheme of the optimum STAP receiver.](image)

FIGURE 1. Block scheme of the optimum STAP receiver.

III. OPTIMUM PHASE-ONLY STAP

The optimum adaptive STAP radar is based on the use of the disturbance covariance matrix in the filter design arising from maximizing the SINR over all possible complex vectors of size \( N \), viz. \( \mathbf{w} \in \mathbb{C}^N \). The Phase-only STAP tries to estimate the complex vectors \( \mathbf{w} \) constraining its elements to have unit amplitude, that is the complex weight vectors is enforced assuming the following form

\[
\mathbf{w} = \begin{bmatrix} e^{j\phi_1}, e^{j\phi_2}, \ldots, e^{j\phi_N} \end{bmatrix}^T.
\]

Therefore, the phase-only weight vector is obtained as the solution to the following optimization problem

\[
\mathcal{P} \left\{ \mathbf{w}_{PO} = \arg \max_{\mathbf{w}} \left( \frac{\|\mathbf{w}^\dagger \mathbf{v}\|^2}{\mathbf{w}^\dagger \mathbf{M} \mathbf{w}} \right) \right. \text{ s.t. } \mathbf{w} \in \mathbb{T}^N \}
\]

namely as the vector maximizing the SINR over the \( N \)-torus.

As already said this paper extends a previous work that focused on adaptive spatial-only nulling [35] to the more general framework of STAP. As highlighted in [35], the phase-only case does not admit a closed-form solution to the constrained optimization problem. The identical challenge exists for phase-only STAP because, unlike the fully optimal case, there is not a closed-form solution to Eq. (9). This is pictorially represented in Figure 2 for a phase-only STAP weight composed by only two array elements transmitting two radar pulses. The space of a phase-only element comprising two antenna elements and two pulses cannot be visually represented because of the four involved phases, however it can be graphically drawn by means of an unfolded torus (which is a projection of the SINR from the space of the four phases in a three-dimensional space in which the
variation is due to only two phases), representing the SINR variation with respect to \( \phi_2 \) and \( \phi_3 \) having set, in this case, \( \phi_4 = 0 \) and \( \phi_1 = [0, \pi/4, \pi/2] \). The unfolded torus clearly emphasizes the presence of many maxima in the overall \( N \) torus and the consequent impossibility in finding a closed-form optimal solution. For these reasons in the following phase-only STAP is solved by introducing a generalization of the CGM provided in [35] to this specific problem. The phase-only STAP can be represented by means of the block scheme of Figure 3 in which the differences with the optimum adapted STAP are clearly either evident. Precisely, the weight vector is computed applying the CGM as described in the following, and then the signal’s samples are phase shifted by the amount of tuning contained by the optimal phase-only weights.

To simplify the mathematical derivations as well as to easily distinguish the phase-only SINR from the fully-adapted, this latter is expressed as

\[
\text{SINR}_{\text{PO}} = \sigma (w) = \frac{w^\dagger S w}{w^\dagger M w}, \quad w \in \mathbb{T}^N, \tag{10}
\]

with \( w \) defined in (8) obtained as the solution to (9) and \( S = vv^\dagger \).

Before proceeding further, some considerations about the phase-only strategy will be discussed. In particular, it is worth recalling that some other solutions for adaptive radar based on the exploitation of the Lagrange multipliers or a specific modification of the eigenvalue analysis of the weight vector can be found [38, p. 286], [39]. These methods can be solved through iterative minimization algorithms such as random search or simplex method, even if they might be inefficient and computationally expensive. Therefore, as in [35], the phase-only STAP problem is solved by means of an innovative optimization algorithm that is the phase-only CGM, obtained by adapting Riemannian optimization methods [40]–[43] to this context. Because this algorithm is based on the evaluation of the gradient of the SINR, in the following subsection the Taylor series expansion of the phase-only SINR derived in [35] is included.

**A. PHASE-ONLY SINR’S TAYLOR EXPANSION AND GRADIENT COMPUTATION**

In this subsection the phase-only SINR’s Taylor expansion for STAP is provided in order to allows the derivation of the phase-only SINR gradient. It is worth noticing that the SINR of a phase-only STAP has the same structural form to that of a spatial-only adaptive array radar. Nevertheless, it must be noted that all the involved quantities (viz. steering vector, weight vector, and covariance matrix) differ in form from their spatial-only counterparts. After this premise, in the following the main steps involved in the derivation of the SINR’s Taylor series are provided. However, the interested readers can refer to [35] for all mathematical derivations and proofs.

Consider the effect of small phase perturbations on the phase-only weight vector \( w \), that is,

\[
w \rightarrow e^{i\Delta w}, \tag{11}
\]

where \( \Delta = \text{Diag} ([\delta_1, \ldots, \delta_N]) \), with \( \delta_1, \ldots, \delta_N \) the perturbations of the phases \( \phi_1, \ldots, \phi_N \).

Now, the SINR in (10) can be separately treated in its numerator \( N(w) \) and denominator \( D(w) \), whose perturbed versions are \( N(e^{i\Delta w}) = w^\dagger e^{-i\Delta} S e^{i\Delta} w \) and \( D(e^{i\Delta w}) = w^\dagger e^{-i\Delta} M e^{i\Delta} w \), respectively. Then, the Taylor expansion series for the numerator and the inverse of the denominator is given by [35]

\[
N(e^{i\Delta w}) = w^\dagger (S - j[\Delta, S] - (1/2)[\Delta, [\Delta, S]] + \ldots) w \tag{12}
\]

and

\[
\frac{1}{D(e^{i\Delta w})} = \frac{1}{w^\dagger M w} + w^\dagger \left( j[\Delta, M] + \frac{1}{2} [\Delta, [\Delta, M]] \right) w (w^\dagger M w)^{-2} - \left( w^\dagger [\Delta, M] w \right)^2 (w^\dagger M w)^{-3} + \ldots \tag{13}
\]
The gradient can be directly computed as shown in the following.

The gradient of \( \sigma(w) \) is obtained as the ratio

\[
\sigma(e^{\Delta w}) = N(e^{\Delta w}) / D(e^{\Delta w}),
\]

where the numerator and the inverse of denominator are given in (12) and (13), respectively. Then, extracting the first order terms of the Taylor series expansion with respect to \( \Delta \), and after some algebraic manipulations, the gradient becomes

\[
\nabla \sigma(w) = \frac{1}{w^\dagger M w} \text{Im} \left\{ \text{diag} \left( [S - \sigma(w)M, ww^\dagger] \right) \right\}. \quad (15)
\]

Exploiting the property that the phase-only SINR is invariant under the transformation \( w \rightarrow e^{i \theta} w \), its gradient in (15) can be computed as [35]

\[
\nabla \sigma(w) = 2 \left( \text{Im} (\alpha^* v \circ w^*) - \sigma(w) \text{Im} (b \circ w^*) / \gamma \right), \quad (16)
\]

where \( \alpha = w^\dagger v, b = M w, \) and \( \gamma = w^\dagger b. \) It is worth to note here that, even if from a structural point-of-view (16) is equal to (32) in [35], the involved quantities significantly differ in the two equations.

**B. CONJUGATE GRADIENT METHOD FOR PHASE-ONLY STAP**

Having derived the SINR’s gradient in the previous subsection, it can be now properly used to solve the optimization problem \( \mathcal{P} \) in (9) through algorithms based on the exploitation of first-order derivatives. Therefore, following the line of reasoning of [35], the CGM [44, p. 625] is applied optimizing on lines on the \( N \)-torus in place of lines in the Euclidean space, that is

\[
w + td \rightarrow e^{i \text{Diag}(d) \cdot w}, \quad (17)
\]

where \( w \) is the phase-only weight vector, \( d \) is the direction, and \( t \) is the step size. Note that, the structure of the lines in the \( N \)-torus space in (17) derive from the fact that the involved perturbations of the weight vector act on its phases.

The CGM for computing phase-only optimum weights for STAP radars can be summarized by the steps described in Algorithm 1.

The algorithm starts with the initialization of the phase-only weight vector \( w_0 \), i.e. belonging to the \( N \)-torus. It is here worth to recall that the phase-only SINR shares many local maximum, as can be observed from the simplest case depicted in Figure 2. As a consequence, the method is strongly influenced by its initial point, that can be set for simplicity as the optimal choice in the quiescent STAP, \( w_0 = v \). The convergence of this algorithm for the computation of phase-only weights has already be proved by simulation in [35], therefore in the Section IV we directly exploits those results. Nevertheless, different initializations of the algorithm can be considered. In particular, an alternative initializer could consist in the use of the clairvoyant target spatial steering vector of size \( M \) with a random Doppler steering vector of size \( M \) drawn from some suitable distribution or the clairvoyant target Doppler steering vector of size \( M \) with a random spatial steering vector of size \( M \). The robustness of the CGM algorithm with respect to the initialization point is studied in Section IV. The other point that merits some further clarifications is that regarding the step size evaluation \( t \). In fact, the considered searching problem is framed within the context of geometric algorithms. It consists in defining a line or, in this case, a geodesic on the torus and efficiently searching for the maximum (or minimum) along it (viz., 1D optimization along the line). This can be done utilizing many line search algorithms, as for instance Wolf-Powell. See [40], [43] in the context of geometric algorithms. As to the computational complexity required by Algorithm 1, note that to compute the updated search direction \( d_{i+1} \) it requires \( 2ML \) real floating-point operations (flips). Moreover, each iteration requires \( 8M^2L^2 \) flips for matrix-vector multiplication and \( 27ML \) flips to compute the gradient (without the computation for \( Mw \)). Finally, in practical context, the covariance estimation is made with \( 4KM^2L^2 \) flips, with \( K \) the number of snapshots used in the estimation process.

To conclude, the Newton’s method could be also applied in this context. However, from a structural point of view, its formalization for the phase-only STAP is the same as
the adaptive array in [35], in this paper we omit this discussion, inviting the interested readers to deepen the works in [35], [45].

IV. PHASE-ONLY STAP PERFORMANCE

This section is devoted to the analysis of the phase-only STAP described in Section III whose solution is found by the CGM given in subsection III-B. First, tests are conducted on simulated data analyzing the SINR at the space-time filter output and the corresponding receiving normalized beampattern (i.e., the radar angular-Doppler response) when the second-order interference statistics are perfectly known. Furthermore, the more realistic case of unknown covariance matrix is then considered to verify the validity of the Reed-Mallet-Brennan rule [36] for the phase-only STAP. Finally, the impact of a limited number of available bits to represent the quantized phases is also studied.

A. SINR AND BEAMPATTERN EVALUATION FOR KNOWN INTERFERENCE

The SINR at the space-time filter output is adopted as a performance metric considering the fully adaptive STAP and the quiescent beampattern (also referred to as nonadapted STAP). The radar system is a uniform linear array (ULA) of \( L \) elements with spacing between the antennas of \( d = \lambda_0/2 \), where \( \lambda_0 \) is the radar operating wavelength.

The SINR is given in (6), whereas the beampattern is defined as

\[
\text{BP} = \left| w^H v(\nu, \theta) \right|^2. \tag{18}
\]

The inference scenario comprises several contributions associated with different interference sources: system noise, clutter (associated with the echoes from the specific operating environment), and jammers (intentional disturbances impinging on the radar antennas). Therefore, the interference covariance matrix is given by [2]

\[
M = M_C + M_J + \sigma_n^2 I,
\]

where \( M_C \) is the covariance associated with clutter components, \( M_J \) the matrix accounting for jammers, and \( \sigma_n^2 \) is the actual system noise power level assumed uncorrelated. The clutter covariance matrix is

\[
M_C = \sigma_C^2 M_{Ct} \otimes M_{Cs}, \tag{19}
\]

where the temporal component is Gaussian shaped

\[
M_{Ct}(h, l) = \rho_C^{[h-l]^2} e^{2\pi(h-l)v_{Dc}},
\]

\[
h = 1, \ldots, M, \ l = 1, \ldots, M, \tag{20}\]

and the spatial component is exponentially shaped

\[
M_{Cs}(h, l) = \rho_C^{[h-l]},
\]

\[
h = 1, \ldots, L, \ l = 1, \ldots, L, \tag{21}\]

with \( \sigma_C^2 \) the clutter power, \( v_{Dc} \) the normalized clutter Doppler frequency, and \( \rho_C \) the clutter temporal and spatial correlation coefficients, respectively.

The jammer covariance matrix is

\[
M_J = \sigma_J^2 I \otimes (v_J(\theta_J)v_J(\theta_J)^H), \tag{22}\]

with \( \sigma_J^2 \) being the jammer power, \( \theta_J \) the angle of boresight of the jammer, and \( v_J \) the jammer steering defined as in (1).

The first study refers to a radar system comprising \( L = 8 \) antennas and transmitting a coherent burst of \( M = 8 \) pulses. The target echo impinges on the radar receiver with a direction of arrival (DOA) equal to \( \theta_{t_0} = 25 \) degrees and moving towards the radar with a normalized Doppler of \( v_{Dt_0} = 0.4 \). The interfering environment is characterized by the parameter values summarized in Table 1.

**Table 1. Parameters of the interfering scenario for the first study case.**

| \( \sigma_n^2 \) | \( \sigma_C^2 \) | \( v_{Dc} \) | \( \rho_C \) | \( \rho_{Ct} \) | \( \sigma_J^2 \) | \( \theta_J \) |
|----------------|----------------|-----------|-------------|-------------|-------------|--------|
| 0 dB           | 40 dB          | 0         | 0.95        | 0.95        | 40 dB       | 50 degrees |

Figure 4 reports the normalized beampattern of the phase-only STAP also in comparison with those of the fully-adapted STAP, the nonadapted STAP, the phase-only in temporal domain, \( \Psi_{PO,t} = \Psi_t \otimes \Psi_s \) (with \( \Psi_t \) the optimum phase-only temporal weight vector), the phase-only in spatial domain, \( \Psi_{PO,s} = \Psi_t \otimes \Psi_s \) (with \( \Psi_s \) the optimum phase-only spatial weight vector), the phase-only evaluated in the two disjoint domains, \( \Psi = \Psi_t \otimes \Psi_s \), the phase of the fully adaptive filter, \( \Psi_{FA,phase} = e^{iM^H y} \), and the semidefinite relaxation (SDR) method of [46]. Additionally, the interference power is also plotted so as to have a complete frame of the effectiveness of the considered approach. The pictures reveal that the phase-only STAP is capable to concentrate the power of the main-lobe in correspondence of the target position in terms of both angle and normalized Doppler (target position is indicated with the black x in the 2-D patterns). Additionally, phase-only STAP is capable of properly canceling the interference contribution by placing deep nulls in correspondence of them, as can be seen by comparing that figure with the interference power of subplot d). Comparing subplots a) and b) it is quite evident that phase-only STAP exhibits a reduced performance degradation with respect to the fully optimum STAP. From inspection of subplots d) and e), it is quite evident that the spatial and temporal phase-only alone do not give satisfactorily performances in the joint domain, i.e., if a proper cancellation is performed in the interfering angular direction, it is not done for Doppler frequency and vice-versa. Some improvements are however given by using the disjoint phase-only STAP, even if it is not able to reach the same performance as the phase-only STAP directly derived in the joint domain. Again, subplot g) demonstrates that the filter based on the phases of the fully adapted have some performance degradation with respect the fully adapted one essentially confined to the missing cancellation of the
spatial jammer. Finally, subplot (e) is related to the SDR which is quite capable of correctly point towards the target and putting deep nulls in the direction/Doppler of interference, even if its shape is not very close to that of the fully adapted in some zones of the angle/Doppler map. Finally, as is well known, the unadapted filter cannot remove the interference despite correctly pointing towards the target.

To further understand the behavior of the proposed phase-only STAP, Figure 5 depicts the SINR values (expressed in dB) in the angle-Doppler map for the same interfering scenario as in Figure 4. The figures show some performance losses in the phase-only STAP with respect to the fully-adapted that can be essentially motivated by the fact that the steering points at $\nu$ adapted that can be essentially motivated by the fact that the steering points

$$n = M + J \sigma_n^2$$

with

$$J = \begin{bmatrix} M & 0 \\ 0 & L \end{bmatrix}$$

and

$$\sigma_n^2 = \begin{bmatrix} \sigma^2 \end{bmatrix}$$

as given in Figure 6, the phase-only and fully-adapted STAP reach exactly the same SINRs.

To better emphasize the effectiveness of the phase-only STAP a clutter model comprising clutter edge is also considered in the next simulation. Precisely, Fig. 7 shows the beampattern for the phase-only and optimum adapted STAP assuming the target located at 0 degrees in azimuth with a normalized Doppler frequency of 0.33 and for the interfering scenario whose relative power is illustrated in Fig. 7(c). The interfering scenario is the same as in Fig. 23 of [2], where two jammers are considered having azimuth angles equal to $-40$ degrees and 25 degrees, respectively, whereas the stationary clutter is modeled as composed by 360 patches.

The considered radar system is composed by an array of $M$ elements and for each considered pulse with respect to the studied receiving filter with respect to the nonadapted STAP. The 2D diagrams clearly highlight the phase variation over the array toward a position different from 0 degrees and even if its shape is not very close to that of the fully adapted scenario of the first study case described by means of Figure 4. However, now the histograms of the sidelobes are computed having removed first the mainlobe from the related beampattern as shown in Figure 9. The areas that identify the mainbeam within the phase-only and fully-adapted beampatterns are highlighted by the green box in subplots (a) and (b), respectively, selected with the same extent in this study. Moreover, subplot (c) of the same figure compares the two sidelobes histograms. Observing these representations, the evidence is that the phase-only STAP has slightly higher sidelobes than the fully-adapted counterpart. Nevertheless, the histogram is mostly concentrated (in the simulation study) around $-40$ dB with respect to the peak value, that represents a quite satisfactory value within contexts of practical interest.

C. PHASES ANALYSIS

This subsection is aimed at studying the effect of quantization, i.e. impact of a finite number of bits [38], used in the digital implementation and storage of the phase-only weight vectors. To do this, in Figure 10 the SINR values at target position are plotted as a function of the number of bits used to represent the phases in the weight vector $w_{PO}$ for the same interfering scenario as Figure 4.

The curves clearly highlight the losses suffered by the phase-only STAP receiver in utilizing a low number of bits to quantize the involved phases. Precisely, the SINR evaluated for different numbers of antenna and different numbers of pulses, viz. $(L = 8, M = 8), (L = 8, M = 16), (L = 16, M = 8)$, grows as the utilized number of bits increases, approximately reaching its maximum value for 10 bits. This latter represents an interesting result since the phase-only weight vector can be represented without losses with a relatively low number of bits available in commercial devices. As to the maximum SINR value observed in this figure, as highlighted before, it is essentially due to the steering of the radar toward a position different from 0 degrees and 0 Doppler.

Figure 11 depicts the behavior of the phases for the optimum phase-only STAP weight vector (and those of its competitors) considering a phased-array comprising $L = 8$ elements and transmitting a burst of $M = 8$ pulses. More specifically, Figures 11(a) to 11(d) depict the contour plots of the 2D (two-dimensional) phases for the phase-only initialized with $v$, the phase-only initialized with $w_0 = x_i \otimes v_i$, the phase-only initialized with $w_0 = v_i \otimes x_i$, and the phase of fully-adapted, respectively. Additionally, Figures 11(e) to 11(h) report the 2D phase difference of each studied receiving filter with respect to the nonadapted STAP. The 2D diagrams clearly highlight the phase variation over the array elements and for each considered pulse with respect to the classic counterpart.

D. PRACTICAL IMPLEMENTATION TESTS

The first test is performed to assess the validity of the Reed-Mallet-Brennan rule [36] for the phase-only STAP. The developed tests consists in evaluating the achievable SINR in a more realistic situation in which the disturbance covariance matrix is not known a-priori. In this respect, it is
assumed the availability of range data (secondary/training data or snapshots) close to the cell under test, that are hypothesized of being stationary, homogeneous, and target free. Additionally, these data share the same statistical distribution as the primary datum, and the sample covariance matrix (SCM), that represents the maximum likelihood (ML)
Estimate in homogeneous Gaussian environments [36], [47], is used in place of the true covariance in STAP evaluation. For a number of snapshots approximately greater than two-times the matrix size \( N \) herein), the SCM is capable of ensuring a SINR performance loss of only 3 dB on average with respect to the optimum [36]. After this premise, let us consider \( K \) training data, \( r_1, \ldots, r_K \), modeled as \( N \)-dimensional independent zero-mean complex circular Gaussian vectors with the same positive definite covariance matrix \( M \) as the primary datum. Under this circumstance, the joint probability density function (pdf) of the snapshot is

\[
f(r_1, \ldots, r_K | M) = \frac{e^{-\text{tr}(M)^{-1} S}}{\pi^{NK} |\det M|} \]  

where

\[
S = \frac{1}{K} \sum_{k=1}^{K} r_k r_k^\dagger.
\]
Figure 9 shows the SINR at target position versus number of bits for the scenario of Figure 4. Figure 12 shows the SINR achieved by the phase-only STAP using the SCM in place of true covariance for the interfering scenario of Figure 4(d) evaluated at the target position. The curves are plotted as function of the number of snapshots and different number of bits to quantize the phases of the estimated weight vector. From a first visual inspection, as expected, the SINR increases as the number of snapshots and contextually showing restrained performance losses with respect to the optimum phase-only STAP, i.e. that assuming the perfect covariance knowledge. As a matter of fact, for a number of secondary data equal to $K = 3N = 192$, the phase-only STAP with the SCM shows a SINR loss of only less than 1 dB with respect to its optimum counterpart, when a sufficient number of bits is available at the receiver. Additionally, under the challenging situation $K = N = 64$, the phase-only STAP using the SCM is able to reach SINR values whose amount of reduction is still contained in the $-3$ dB limit. Finally, as already observed in the analysis of Figure 10, the use of only 8 bits in the phase coding is not sufficient to provide satisfactorily performances in terms of target detection as well as interference cancellation.

Finally, we study the computational burden of the phase-only STAP considering as figure of merit the elapsed time needed to estimate the weight vector. In this respect, the test is conducted on an Intel(R) Core(TM) i5-8250U CPU @1.60GHz 1.80GHz, RAM 16 GB, whose results are graphically reported in Figure 13 varying the number of pulses (for $L = 8$ array elements) and then the number of array elements (for $M = 8$ pulses). Moreover, as for the other tests, the number of iterations for the CGM algorithm is set equal to 50, having observed that it ensures the convergence. The results emphasize that the elapsed time increases with either the number of pulses or array elements even if it is contained below 0.08 s also in the worst case. For comparison purposes, the optimum fully-adapted STAP is also considered, whose computational time is strictly related to the time needed to perform matrix inversion.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure9.png}
\caption{Sidelobes’ histogram of the phase-only STAP and fully-adapted STAP. Subplots refer to a) phase-only and b) optimum-adapted SINR with emphasized the removed mainlobe for the computation of the histograms. Subplot c) instead shows the two sidelobes histograms.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure10.png}
\caption{SINR at target position versus number of bits for the scenario of Figure 4.}
\end{figure}

\begin{equation}
\text{SINR} = \frac{\|w^\dagger((c \odot v_l(\nu D)) \otimes v_j(\theta))\|^2}{w^\dagger M_w w}, \quad (26)
\end{equation}

where the numerator is the useful energy at the output of the filter (tuned to the nominal target Doppler frequency and angular direction), while the denominator represents the signal-dependent disturbance energy at the output of the filter, with $M_w$ the signal-dependent disturbance covariance matrix. According to the previous guidelines given in Section III, the phase-only weights $w$ can be found using the SINR in (26) as objective function to maximize. Results of this analysis
FIGURE 11. Phases of the STAP weight vector for an array of $L = 8$ elements transmitting $M = 8$ coherent pulses. Subplots on the top are the phases contour plot and those on bottom are the phase variation for each filter with respect to the nonadapted of a)-e) phase-only initialized with $v$, b)-f) phase-only initialized with $w_0 = x_t \otimes x_s$, c)-g) phase-only initialized with $w_0 = x_t \otimes x_s$, and d)-h) phase vector of fully-adapted.

FIGURE 12. SINR versus number of snapshots, $K$, for a radar STAP with an array of $L = 8$ elements transmitting $M = 8$ coherent pulses, that is $N = 64$. are reported in Figures 14(a) to 14(c) in terms of normalized beampatterns for the phase-only STAP in comparison with the fully-adapted and the spatial phase-only previously introduced. Precisely, a radar composed by $L = 16$ array elements and transmitting a Barker code of length $M = 20$ is used. Four interfering sources from directions $\theta = [0, 10, -40, 40]$ degrees and with normalized frequencies $\nu_D = [-0.325, 0, 0.325, 0.325]$ are considered, as depicted in Figure 14(d). From figures’ observation, the similarity between phase-only and fully-adapted beampatterns appears to be quite evident. Moreover, the spatial phase-only is not capable of ensuring a satisfactorily cancellation of all interferences.

F. JOINT PHASE-ONLY STAP AND TRANSMITTING WAVEFORM OPTIMIZATION

This last section provides a method for jointly optimizing the transmitted waveform and the receiving filter to improve the target detection constraining both of them to have unit-modulus (i.e., to be phase-only vectors). In particular, assuming the signals embedded in Gaussian interference, this results is achieved choosing the radar waveform and the receive filter that maximizes the SINR $\sigma(w, p)$, that is

$$\mathcal{P}_1 \left\{ \begin{array}{c} \arg \max_{w, p} \frac{\left| w^T p \right|^2}{w^T M w} \\ \text{s.t.}, \quad w \in \mathbb{T}^N, \\ p \in \mathbb{T}^N, \end{array} \right. \quad (27)$$

where $p$ is the radar transmitted waveform and $M$ is the signal-independent disturbance covariance. Now, following the line of reasoning of some already published papers [25], [30], [33], [56], an iterative and alternating optimization approach is herein implemented. Precisely, at each step only...
one variable is optimized while the other is maintained fixed, and vice versa at the next step. Therefore, assuming fixed the waveform, the weight vector is optimized then, at the successive stage, the waveform is optimized maintaining fixed the weight vector optimized at the previous iterative step. Note that, the optimization of the waveform is exactly performed as described in Algorithm 1 of Section III.B, whereas that of the waveform is done applying the phase-only CGM of Algorithm 1 with the only difference in the computation of the SINR gradient. More in details, indicating with $e^{i\Delta p}$ a perturbed version of the phase-only waveform $p$, the Taylor series expansion of $\sigma(w, p)$ in (27) with respect to $\Delta$, up to the first order, results to be

$$\sigma(w, e^{i\Delta p}) = \sigma(w, p) - \frac{\partial}{\partial w} \sigma(w, p) |_{p=0} \Delta,$$

(28)

where $W = ww^\dagger$, and its gradient is

$$\nabla \sigma(w, p) = 2\text{Im}(\beta^* w \otimes e^p) / \gamma,$$

(29)

where $\beta = w^\dagger p$.

The considered simulation setting comprises a disturbance covariance matrix as in (19), whereas the considered radar system is composed by an array of $L = 16$ elements and transmitting a Barker code of length $M = 20$. The starting point of the CGM is the vector $p_0 = (c \otimes n_j(v_D)) \otimes v_s(\theta)$. Figure 15 shows the normalized beampattern for the joint waveform/weight vector phase-only STAP (indicated as joint phase-only), the phase-only STAP, and the fully-adapted STAP. Interestingly, the joint phase-only put a deeper null in the jammer direction with respect to the phase-only STAP. Moreover, the SINR achieved by applying this new approach increases as the number of iteration in the alternate optimization increases, as shown in Figure 15(d).

V. CONCLUSION AND WAY AHEAD

This paper has addressed the problem of deriving the phase-only optimal weight vector for STAP. More precisely, the paper has extended a previous work [35], specifically focused on the adaptive spatial-only nulling, to the jointly space-time domain, i.e. the phase-only STAP. Differently, from the optimal fully-adapted STAP, in which the complex weight vector belongs in general to the complex field, in the phase-only STAP the weight vector is constrained to be within the so-called $N$-torus of phase-only complex vectors. Therefore, the problem has been formulated as a constrained maximization problem, with objective function the output SINR and with the constraint on the weight vector to be a phase-only complex vector. The solution to the corresponding constrained optimization problem has been derived by means of the phase-only CGM, due to the lack of a closed-form solution to it. Several numerical case studies have verified the effectiveness of the phase-only STAP in terms of both SINR values and receiving beampattern. The method has also been compared with the optimum fully-adapted STAP used as performance benchmark as well as other possible competitors. Finally, analyses of some practical utility have been performed to demonstrate possible pros and cons of this method.

Future research tracks might concern the application of numerical simulations in other scenarios of practical interest in the radar field as well as the validity of the proposed framework to measured radar data.

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