A kinematic excess in the annular gap and gas depleted cavity in the disc around HD 169142
H. Garg, C. Pinte, I. Hammond, R. Teague, T. Hilder, D. J. Price, J. Calcino, V. Christiaens, P. P. Poblete

To cite this version:
H. Garg, C. Pinte, I. Hammond, R. Teague, T. Hilder, et al.. A kinematic excess in the annular gap and gas depleted cavity in the disc around HD 169142. Monthly Notices of the Royal Astronomical Society, 2022, 10.1093/mnras/stac3039 . insu-03860272
A kinematic excess in the annular gap and gas-depleted cavity in the disc around HD 169142

H. Garg 1, 2, 3, 5, C. Pinte 1, 2, I. Hammond 1, R. Teague 1, 3, 4, T. Hilder, D. J. Price, J. Calcino, V. Christiaens 6 and P. P. Poblete 7, 8

1 School of Physics and Astronomy, Monash University, Clayton VIC 3800, Australia
2 CNRS, IPAG, Univ. Grenoble Alpes, F-38000 Grenoble, France
3 Department of Earth, Atmospheric, and Planetary Sciences, Massachusetts Institute of Technology, Cambridge, MA 02139, USA
4 Center for Astrophysics | Harvard & Smithsonian, 60 Garden Street, Cambridge, MA 02138, USA
5 Theoretical Division, Los Alamos National Laboratory, Los Alamos, NM 87545, USA
6 Space sciences, Technologies & Astrophysics Research (STAR) Institute, Université de Liège, Allée du Six Août 19c, B-4000 Sart Tilman, Belgium
7 Astrophysikalisches Institut, Friedrich-Schiller-Universität Jena, Schillergäßchen 2-3, D-07745 Jena, Germany
8 Núcleo Milenio de Formación Planetaria (NPF), Chile

Accepted 2022 October 14. Received 2022 October 2; in original form 2022 April 5

ABSTRACT

We present ALMA band 6 images of the 12CO, 13CO, and C18O J = 2-1 line emissions for the circumstellar disc around HD 169142, at ~8 au spatial resolution. We resolve a central gas-depleted cavity, along with two independent near-symmetric ring-like structures in line emission: a well-defined inner gas ring [∼25 au] and a second relatively fainter and diffuse outer gas ring [∼65 au]. We identify a localized super-Keplerian feature or vertical flow with a magnitude of ∼75 ms⁻¹ in the 12CO map. This feature has the shape of an arc that spans azimuthally across a position angle range of ∼60° to 45° and radially in between the B1[26au] and B2[59au] dust rings. Through reconstruction of the gas surface density profile, we find that the magnitude of the background perturbations by the pressure support and self-gravity terms are not significant enough to account for the kinematic excess. If of planetary origin, the relative depletion in the gas-density profile would suggest a 1 Mj planet. In contrast, the central cavity displays relatively smooth kinematics, suggesting either a low-mass companion and/or a binary orbit with a minimal vertical velocity component.

Key words: accretion, accretion discs – circumstellar matter – stars: individual: HD169142 – submillimetre: planetary systems.

1 INTRODUCTION

High-resolution imaging of discs around pre-main-sequence stars by the ALMA (Atacama Large Millimeter/submillimetre Array) interferometer has revealed substructures in the form of gaps and rings primarily seen in dust emission (e.g. ALMA Partnership 2015; Andrews et al. 2016, 2018; Sierra et al. 2021). One popular mechanism for the formation of concentric rings is the dynamical interaction of the disc with embedded planets (e.g. Ayliffe et al. 2012; Pinilla, Benisty & Birnstiel 2012; Dipierro et al. 2015; Dong, Fung & Chiang 2016; Rosotti et al. 2016; Dong & Fung 2017; Veronesi et al. 2020). Alternatives include magnetohydrodynamic instabilities (e.g. Flock et al. 2015; Pinilla et al. 2016) and condensation fronts (e.g. Kretke & Lin 2007; Saito & Sirono 2011; Zhang, Blake & Bergin 2015; Okuzumi et al. 2016).

Embedded planets have long been predicted to perturb the gas component of the disc (Rafikov 2002). The gravitational force exerted by the planet on the natal disc results in the formation of density waves launched at Lindblad resonances that superimpose to resemble a coherent wake propagating away from the location of the planet. This translates to local deviations in the otherwise uniform velocity fields, which gradually diminish in magnitude with increasing distance from the planet. The magnitude of the deviations is directly correlated to the mass of the perturbing planet (e.g. Bollati et al. 2021).

Empirical methods based on gas kinematics are becoming a common practice to indirectly infer the presence of an embedded planet (Pérez, Casassus & Benítez-Llambay 2018). Planets can carve gaps in the gas density profile and the associated pressure gradients can manifest as velocity perturbations which can indirectly reveal the presence of the planets (Teague et al. 2018). Specifically, the local density depletion equates to negative and positive pressure gradients along the boundaries, which translate to sub- and super-Keplerian rotation with respect to the background Keplerian profile, respectively. While this observation is independent of the underlying mechanism responsible for the generation of the gaps, velocity deviations closely resembling a wake favour a planetary origin. Deviations in velocity channels (kinks) from the expected isovelocity curves can also be used to infer the presence of a planet, especially when the location of the gas signature correlates well with the dust gaps (e.g. Pinte et al. 2019). Acquiring the gas surface density profile allows for the computation of the background rotational velocity profile for a pressure-supported disc. Furthermore, as an alternative approach to kinematics, the magnitude of the relative depletion within a dust gap can also be directly correlated to planetary masses expected to carve such a gap (e.g. Kanagawa et al. 2015; Dong & Fung 2017; Bae, Pinilla & Birnstiel 2018; Lodato et al. 2019; Bollati et al. 2021).

© 2022 The Author(s) Published by Oxford University Press on behalf of Royal Astronomical Society
HD 169142 is a Herbig Ae star with an estimated mass of $M_*=1.65M_\odot$ (Blondel & Dje 2006), luminosity $L_*=10L_\odot$ (Fedele et al. 2017), and an effective temperature of $T_*=8400$ K (Dunkin, Barlow & Ryan 1997), located at a distance of $117 \pm 4$ pc away (Gaia Collaboration 2016). The disc encircling this star is oriented nearly face-on at an inclination of $13^\circ$ (Raman et al. 2006; Pančić et al. 2008) and a position angle (PA) of $5^\circ$ for the major axis (Raman et al. 2006). This disc is one of many to comprise of distinct ring-like structures ($r \sim 25$ au and $\sim 65$ au) and a central cavity ($R_{\text{c}} \sim 22$au) as seen in scattered light (Quanz et al. 2013; Momose et al. 2015; Pohl et al. 2017; Bertrang et al. 2018); thermal mid-infrared (Honda et al. 2012); millimetre/submillimetre with ALMA (Fedele et al. 2017; Macías et al. 2019; Pérez et al. 2019); and centimetre with the VLA (Very Large Array) (Osorio et al. 2014). At higher spatial resolution the outer ring was resolved into three independent rings with radial separations of $\sim 10$ au (Pérez et al. 2019). High-contrast imaging has revealed various point-like sources along the inner and outer edges of the innermost ring (Billier et al. 2014; Reggiani et al. 2014; Ligi et al. 2018; Gratton et al. 2019), but the close overlap of these features with the dust ring prevented an unequivocal conclusion on the presence of embedded planets (Billier et al. 2014; Ligi et al. 2018). Exterior to the dust rings, signatures of meridional flows have also been reported at a radius of 125 au (Yu et al. 2021).

In this paper, we present ALMA band 6 observations of the disc around HD 169142 for the $^{12}$CO, $^{13}$CO, and $^{18}$O $J = 2-1$ line transitions imaged at 0.07 and 0.1 arcsec angular resolutions and 0.167 km s$^{-1}$ spectral resolution, taking into account Hanning smoothing by the correlator. This level of angular resolution allowed us to resolve concentric gas rings in all three line tracers and detect small-scale ($\sim 50$ m s$^{-1}$) velocity perturbations stemming from in between the dust rings.

2 OBSERVATIONS, DATA REDUCTION, AND IMAGING

ALMA band 6 observations of the disc around HD 169142 from Projects [2015.1.00490.S] and [2016.1.00344.S] (hereafter P2015 and P2016) were used to image the 1.3mm thermal continuum emission and the $^{12}$CO, $^{13}$CO, and $^{18}$O $J = 2-1$ rotational line transitions. For specifications of the individual executions per project, refer to Table 1. We calibrated P2015 with the ALMA pipeline using CASA version 4.7.0, while P2016 was pipeline calibrated by the ESO (European Southern Observatory) staff. Prior to self-calibration, visibilities per execution were independently imaged using only the continuum spectral window to determine parameters for phase-centring prior to merging executions with shared antenna configurations. We used the publicly available reduction-utils script by the DSHARP team to (1) determine parameters for phase-centring, which does so by fitting a Gaussian to the inner part of the disc, and (2) determine whether further flux-rescaling was required post-pipeline calibration. We re-scaled executions 1, 2, and 3 from P2015 due to an initial difference of $> 4$ per cent in flux. Finally, prior to self-calibration, we generated three concatenated files with (i) the three individual execution blocks of P2015, (ii) the two executions of P2016 with compact configuration, and (iii) the three executions of P2016 with extended configuration, using CASA task concat.

Self-calibration involved the sequential application of multiple phase-only calibrations to the continuum-only spectral windows (spws), with solution intervals in the order of [length of a scan] > 120 s > 60 s > 30 s > 15 s > 6 s. An additional, amplitude + phase calibration was applied post phase-only calibration with a solution interval equal to the length of an entire scan. The compact (Com) and extended (Ext) configurations from P2016 and singular configuration from P2015 were independently self-calibrated. Following each iteration in self-calibration, the visibilities were imaged to ensure an increase in the peak signal-to-noise ratio (SNR). Continuum peak SNR improved by a factor of $\sim 4$ and $\sim 6$ for P2016 and P2015, respectively. The self-calibration tables were then applied to the corresponding line emission spws. For P2016, calibration tables for continuum spw centred at $\sim 231$ GHz were used to self-calibrate the $^{12}$CO $J = 2-1$ transition, while those for continuum spw centred at $\sim 217$ GHz were used on $^{13}$CO and $^{18}$O. For P2015, calibration tables from the single continuum only spw were applied to all line spws. P2015 has a channel spacing of 61 kHz for the line spws, corresponding to a spectral resolution of 71 kHz, due to the correlator applying Hanning smoothing. Similarly, P2016 has a channel width of 122 kHz for line spws with a channel binning of 4. The product images are the combined products of the individually self-calibrated P2015 and P2016 data sets, where CASA tasks fixpix and fixplanets were used for alignment prior to merging using CASA task concat.

Imaging was performed using CASA task tclean with the multiscale deconvolver and several weighting schemes.
Figure 1. Gas rings, gaps, and cavity. Integrated intensity and peak intensity maps (given in units of brightness temperature) for the $^{12}$CO, $^{13}$CO, and C$^{18}$O $J = 2 - 1$ maps, with and without continuum subtraction. The disc is inclined by $13^\circ$ perpendicular to a PA of $5^\circ$. All maps are imaged at a resolution of 0.07 arcsec with Briggs robustness factor of 0.0 and a uv-taper to circularize the beam, which is displayed on the bottom-left corner.

Figure 2. Thermal continuum emission. (a) superuniform weighted map; (b) slightly degraded resolution with Briggs $r = -0.5$. The overlaid dotted rings represent the locations of the B1[26au], B2[59au], B3[66au], and B4[77au] dust rings as presented in Pérez et al. (2019); (c) continuum emission imaged at a similar spatial resolution to line emission ($\sim$0.07 arcsec).
Figure 3. Azimuthally averaged profiles. (a) non-continuum-subtracted integrated intensities of the $^{12}$CO, $^{13}$CO, and C$^{18}$O $J = 2 - 1$ lines; (b) non-continuum-subtracted peak intensity maps of the $^{12}$CO, $^{13}$CO, and C$^{18}$O $J = 2 - 1$ lines, portrayed in units of brightness temperature. The blue highlighted region marks the freeze-out temperature of CO; (c) superuniform weighted 1.3mm continuum emission; (d) 1.3mm continuum emission imaged for a resolution of 0.07 arcsec, to match spatial resolution of line emission. The shaded regions represent the 1σ uncertainty for the corresponding line colour. The light grey vertical line marks the location of the dust rings (same labels as in Pérez et al. 2019), and the dark grey vertical line marks the location of the gap between the CO rings (G1). The horizontal bar represents the spatial resolution.

(superuniform and Briggs with a few robust parameters). In a few instances, a uv-taper was added in order to smooth emission and circularize the synthesized (clean) beam. Masking was performed using auto-multithresh. Continuum images produced using superuniform weighting, Briggs $r = 0$ and Briggs $r = 0 +$ uv-taper have beams of 0.028 arcsec $\times$ 0.016 arcsec, 0.044 arcsec $\times$ 0.028 arcsec, and 0.065 arcsec $\times$ 0.059 arcsec with an RMS of 0.027, 0.011, and 0.010 mJy beam$^{-1}$, respectively. We image the $^{12}$CO, $^{13}$CO, and C$^{18}$O $J = 2 - 1$ transitions using Briggs weighting with $r = 0$ and a uv-taper resulting in beams of 0.073 arcsec $\times$ 0.067 arcsec, 0.069 arcsec $\times$ 0.063 arcsec, and 0.070 arcsec $\times$ 0.064 arcsec with an RMS of 1.58, 1.39, and 1.06 mJy beam$^{-1}$, respectively (refer to Figs. 1, 2, 3, B1, B4 and B5).

Table 2. Best-fitting parameters from MCMC fitting of the velocity fields in EDDY.

| Keplerian model | | | |
|-----------------|-----------------|-----------------|-----------------|
| PA (°) | $M_*$ ($M_\odot$) | $V_{LSR}$ (ms$^{-1}$) | |
| $^{12}$CO | 5.33 | 1.47 | 6897 |
| $^{13}$CO | 4.96 | 1.49 | 6895 |
| C$^{18}$O | 5.15 | 1.49 | 6886 |

Tapered Keplerian model

| PA (°) | $M_*$ ($M_\odot$) | $V_{LSR}$ (ms$^{-1}$) | $M_{disc}$ ($M_\odot$) | $\gamma$ | $r_{in}$ (°) |
|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| $^{12}$CO | 5.32 | 1.47 | 6895 | -0.59 | 0.37 | 0.70 |
| $^{13}$CO | 4.95 | 1.49 | 6894 | -0.59 | -0.27 | 0.74 |
| C$^{18}$O | 5.17 | 1.49 | 6886 | -0.59 | -0.74 | 0.74 |

3 ANALYSIS METHODS

3.1 Searching for kinematic signatures of companions

For gas flow along circular orbits, the rotational velocity of the gas is given by (e.g. Rosenfeld et al. 2013)

$$\frac{v_r}{r} = \frac{GM_r}{(r^2 + z^2)^{1/2}} + \frac{1}{2} \frac{\partial P_{gas}}{\partial r} + \frac{\partial \phi_{gas}}{\partial r},$$

where (1) is the Keplerian velocity component for a geometrically thick disc, where $r$ is the cylindrical radius and $z$ is the height above the disc mid-plane; (2) is the radial pressure gradient component (where $P_{gas} = P_{gas} T$); and (3) is the self-gravity component, where $\phi_{gas}$ is the gravitational potential of the disc; generally only significant when $M_{disc}/M_* > H/R$. For a typical disc, globally both density and temperature decrease as a function of radius which translates into $\partial P_{gas}/\partial r < 0$, and thus, a global sub-Keplerian profile.

To search for hidden kinematic signatures of an embedded planet(s) in HD 169142 (refer to Figs. 4 and 5), we utilize the software EDDY (Teague 2019), which subtracts a background disc model with parameters determined via the Markov chain Monte Carlo (MCMC) method, where the posteriors explore the azimuthally averaged velocity fields from the observations. We fit for disc centre coordinates ($x_0$ and $y_0$), PA, $M_\odot$, and $V_{LSR}$ using 250 walkers to explore the posterior distribution with a total of 10,000 steps, of which the walkers were found to have converged in less than 500 steps. Disc inclination was kept fixed at 13°. The MCMC fitting was limited to the inner 1.5 arcsec radial range of the disc, because (1) line emission past this radius was found to be more noise dominated, and (2) the gas surface density was also found to drop drastically past the outermost dust ring and thus could have resulted in an underestimation of the stellar mass if included. Additionally, we also mask the inner 0.2 arcsec (2 $\times$ beamwidth) to exclude kinematic biasing from beam smearing. A summary of the best-fitting parameters for all three tracers are listed in Table 2. We refrain from including the associated uncertainties, as the MCMC fitting produces statistically negligible uncertainties for the free parameters. As an alternative, we produce a series of residual velocity maps to assess the significance of variations in PA, $M_\odot$, and inclination for $^{12}$CO (Appendix C; Fig. C1).

From the computed gas surface density profile (Fig. 6) it is evident that past 80 au (0.68 arcsec) the gas rotational profile should be sub-Keplerian due to the negative density gradient. Therefore, in EDDY we also fit for a tapered Keplerian background model following the
methodology outlined in Teague et al. (2022). A tapered Keplerian model follows the form
\[ v_{\text{kep, tapered}} = \sqrt{\frac{G(M_\ast + M_d(r))}{r}}, \]
where \( M_d(r) \) is an effective disc mass set by
\[ M_d(r) = M_{\text{disk}} \times \frac{r^2 \gamma - r_{\text{in}}^2 \gamma}{r_{\text{out}}^2 \gamma - r_{\text{in}}^2 \gamma}. \]
\( r_{\text{in}} \) and \( r_{\text{out}} \) define the inner and outer boundaries where gas rotational velocity deviates from Keplerian, respectively. \( M_{\text{disk}} \) is measured at \( r_{\text{out}} \) (set to 3.0 arcsec in our case) and a negative quantity translates to slowed rotation, mimicking a pressure gradient, while \( \gamma \) determines how quickly the gas rotational profile slams from Keplerian.

Here, we include \( M_{\text{disk}}, \gamma, r_{\text{in}} \) as additional free parameters to the MCMC fitting and provide the best-fitting values in Table 2 for each tracer. To derive the statistical significance of any detected kinematic structure, we divide the residual velocity maps by the statistical uncertainty on the velocity per pixel (\( \delta v_0 \)).

To spectrally collapse line emission, we utilize the BETTERMOMENTS package (Teague & Foreman-Mackey 2018), which returns both the projected peak velocity maps \( (v_p) \) and the statistical uncertainty per pixel (\( \delta v_0 \)). Specifically, we use the Gaussian method to spectrally collapse the cube, as the method has been shown to have minimal statistical uncertainty (Yu et al. 2021).

For the kinematic analysis we use maps with a slightly degraded beam of 0.1 arcsec resolution, using the Briggs robustness factor of 0.5 (instead of 0) to achieve higher sensitivity. Additionally, a uv-taper is also applied to circularize the beam. Due to the low inclination of the disc, the background disc model is assumed to be geometrically thin e.g. no vertical extension \( (z = 0) \). Theoretically, this assumption should result in an underestimation of the true stellar mass (in accordance with equation 1) for the \( ^{12}\text{CO} \) and \( ^{13}\text{CO} \) tracers which are typically more elevated in the disc layers. However, the best-fitting stellar masses of 1.473, 1.488, and 1.487 \( M_\odot \), for \( ^{12}\text{CO}, ^{13}\text{CO}, \text{and } C^{18}\text{O} \), respectively, are found to only differ by \( \sim 1 \) per cent.

To extract the three independent velocity profiles \( (v_g, v_r, v_z) \), we use the \texttt{fit annuli} function in eddy on the line-of-sight velocity maps computed with the Gaussian method.

### 3.2 Computing the gas surface density structure

The upper and lower bounds of the gas column density structure are computed as per the method outlined in Garg et al. (2021), and we refer the reader there for more thorough discussions on caveats and a means of accounting for them. This technique has also been implemented in Lyo et al. (2011), Schwarz et al. (2016), Perez et al. (2015), and Casassus et al. (2021). For completeness, we provide the main formulae in Appendix A. We use the Leiden Atomic and Molecular Database (LAMDA) (Schöier et al. 2005) (accessed in 2020 July), to acquire quantities for the \( E_\nu \) and \( A_{\nu d} \) coefficients in equations (A2) and (A3). The computed molecular column density using equations (A2) and (A3) is scaled to represent total gas column density by multiplying by the canonical ISM abundance ratios: \( [^{12}\text{C}]/[^{13}\text{C}] \approx 70 \) (Stahl, Casassus & Wilson 2008), \( [^{16}\text{O}]/[^{18}\text{O}] \approx 500 \) (Wilson & Rood 1994), and \( [\text{H}_2]/[^{12}\text{CO}] \approx 10^4 \). The total gas column density structure calculated considering either continuum-subtracted or non-continuum-subtracted line maps is presented in Fig. 6. We made no assumption on the level of the individual isotopic depletion in the disc, as the ambiguity in the true line intensity can already lead to an order-of-magnitude uncertainty on the computed column density profile, i.e. the difference between the upper and lower bounds due to continuum subtraction. Additionally, this method of computing the surface density requires that the temperature and density tracing species share the same local temperature. Pinte et al. (2018) demonstrated that the emission heights of the \( ^{13}\text{CO} \) and \( C^{18}\text{O} \) \( J = 2-1 \) surfaces closely overlap, therefore given that we find \( ^{13}\text{CO} \) to be optically thick throughout the disc, we used it as the temperature tracer (rather than \( ^{12}\text{CO} \)), while we used the optically thin \( C^{18}\text{O} \) to derive the column density following Appendix A2.

From the gas column density and temperature maps, we are able to compute the gas rotational profile for a fully pressure-supported disc as well as deduce radial and azimuthal velocity offsets expected from localized pressure gradients. Given that the disc’s gas structure is fairly symmetric, we use an azimuthally averaged gas surface density profile to compute the second term in equation (1) and present the results in Fig. 7.

The gas volume density is computed via
\[ n(r)_{\text{gas}} = \frac{\Sigma(r)}{2\pi h(r)}, \]
where \( \Sigma(r) \) is the gas surface density profile and \( h(r) \) is the hydrostatic scale height given by
\[ h(r) = \sqrt{\frac{r^2 k_b T(r)}{G M_* m_H}}, \]
under the assumption of an isothermal vertical temperature structure. \( k_b \) is the Boltzmann constant, \( G \) is the gravitational constant, \( M_* \) is the stellar mass, \( \mu \) is the mean molecular mass \( (\sim 2.3) \), and \( m_H \) is the mass of hydrogen.

Pressure is given by
\[ P(r) = \rho_N(r) k_{\text{B}} T(r), \]
where \( T(r) \) is equivalent to the azimuthally averaged brightness temperature profile of \( ^{13}\text{CO} \) and \( \rho_N (r) \) is the gas number density. The pressure supported disc model is also subtracted from the line-of-sight velocity map to obtain kinematic residuals independent of localised pressure gradient effects (refer to Fig. 8).

### 3.3 Semi-analytical modelling of the wake

For qualitative comparison of the kinematic features seen in the observations to those induced by an embedded planet, we employ the semi-analytical method of modelling the wake presented in Bollati et al. (2021), with the implementation in WAKEFLOW\(^1\). Via this method, we only consider coplanar orbits and velocity deviations in the plane of the disc, thus neglecting vertical motions. We defer comparisons with full 3D hydrodynamical models for deeper ALMA observations. The semi-analytical model assumes power-law functions for surface density \( (\Sigma) \) and sound speed \( (c) \) profiles, given by
\[ \Sigma_0(r) = \Sigma_\phi (r/r_\phi)^{-d}, \]
and
\[ c_0(r) = c_\phi (r/r_\phi)^{-q}, \]
respectively. Subscript \( p \) denotes estimates at the location of the planet. Here, we use 1.0 and 0.2 for the \( d \) and \( q \) power law indexes; average values derived from fitting to the surface density and brightness temperature profile. The shape of the wake \( (\psi) \) is

\(^1\)https://github.com/TomHilden/wakeflow
inversely proportional to the disc aspect ratio (e.g. $\varphi \propto (h_p/r_p)^{-1}$), which we determine and set to 0.08 (refer to Section 4.4). Models are generated for planetary masses of $1 M_J$ and $10 M_J$, calculated for disc viscosities of $10^{-3}$ and $10^{-1}$, respectively (refer to Sections 4.4 and 5.1 for a more thorough discussion). The planet is placed at an orbital distance of 38 au and PA of 43.8°, as per the location of blob D in Gratton et al. (2019).

The surface density and velocity field calculated by WAKEFLOW are passed to the radiative transfer code MCFOST (Pinte et al. 2006, 2009). The surface density is extended vertically assuming a Gaussian profile with $h(r) = h_0(r/r_0)^{1.25}$, where we set $h_0 = 2.95$ au at $r_0 = 38$ au. We assume that the velocity fields $v_r$ and $v_\phi$ do not depend on the altitude in the disc. We set the total gas mass to $10^{-2} M_\odot$ (Toci et al. 2020) and the gas-to-dust ratio (which is constant across the disc) to 100. We assume a grain size distribution $dn(a) \propto a^{-3.5} da$ between 0.03 μm and 1mm, with a silicate composition (Weingartner & Draine 2001). Dust properties are calculated using the Mie theory. We assume that the disc is passively heated by the star, and use 12.8 millions packets to compute the dust temperature structure. The generated synthetic $^{12}$CO maps have a channel spacing of 32 ms$^{-1}$, assuming the line is in LTE with $T_{\text{gas}} = T_{\text{dust}}$. We use a relative CO abundance of $10^{-4}$ and include CO freeze-out below 20 K, photodissociation, photodesorption (following Pinte et al. 2018). The synthetic cubes are then convolved both spatially (with the observed beam of 0.1 arcsec) and spectrally (with a Hanning function of width 167 ms$^{-1}$). To produce the residual velocity maps from the analytic models, we produce synthetic cubes with MCFOST identical to the set-up above with the exception of the analytic velocity perturbations from WAKEFLOW (refer to Figs. B2 and B3), which are then subtracted from the WAKEFLOW + MCFOST cubes.

4 RESULTS

4.1 Central cavity and rings in line emission

Fig. 1 displays the integrated intensity maps with and without continuum subtraction, and the peak intensity ($I_{\text{peak}}$; portrayed in brightness temperature) maps without continuum subtraction, for the $^{12}$CO, $^{13}$CO, and C$^{18}$O lines. A prominent gas ring (hereafter: R1) encompassing the central cavity is readily observed with all three tracers, along with a second (hereafter: R2) but relatively fainter and diffuse ring further out.

Fig. 2 displays the 1.3mm thermal continuum emission first presented in Pérez et al. (2019), but as self-calibrated and imaged by us, and shown for several more weighting schemes to highlight the variation in dust structure when addressed at different resolutions throughout the paper.

For a quantitative analysis of the extent and widths of the gas rings and gaps/cavities, we deprompted the moment maps assuming an inclination of 13° perpendicular to the semimajor axis of the disc at PA = 5° and applied azimuthal averaging. Profiles of the azimuthally averaged gas integrated flux and $I_{\text{peak}}$ maps, with a comparison to the profiles of continuum emission imaged at superuniform weighting and Briggs $r = 0.5$ weighting with a uv-taper, where the latter more closely matches the resolution of the calibrated line emission, are presented in Fig. 3.

Gas emission towards the disc centre is heavily depleted with a sharp gradient in $^{12}$CO halting at $\sim 20$ au; the location of R1 in $^{12}$CO. Similar characteristics are also seen in the profiles of the optically thinner tracers, $^{13}$CO and C$^{18}$O, but with the peak emission of R1 shifting to larger radii of $r \approx 22$ and $r \approx 26$ au, respectively. Here, the peak of R1 in C$^{18}$O is almost consistent with the profile in continuum emission. The observed narrowing of the central gas cavity ($R_{\text{gas}}$) from C$^{18}$O → $^{13}$CO → $^{12}$CO is due to an optical depth ($\tau$) effect, where a decreasing $\tau$ requires higher column densities before the molecular emitting layer becomes prominent. Hence, peak emission of R1 is seen to shift to an increasing radius from $^{12}$CO → $^{13}$CO → C$^{18}$O, but the subsequent drop in intensity occurs at a similar radius, of $\sim 40$ au, for all three tracers; the first gap (hereafter: G1).

In comparison to R1, the emission from the second gas ring (R2) is found to be more diffuse and shallower in integrated intensity. In non-continuum-subtracted $I_{\text{peak}}$ maps, R2 in $^{12}$CO and $^{13}$CO is seen to be almost two-thirds as bright as R1, while in C$^{18}$O, the brightness temperature of R2 is comparable to R1. This disparity is likely due to the contrast in continuum emission between the two rings.

Given the inherent difference in optical depth between the tracers, the similarities seen between the intensity distributions of all three tracers is instead suggestive that the brightness profile of $^{12}$CO is not solely due to a local enhancement in temperature, instead an accumulation of gas in confined ring structures. Furthermore, the brightness temperature profiles of all three tracers remain above the CO freeze-out temperature ($T_{\text{freeze}} \sim 20$ K) within the inner 200 au radius, suggesting that the location of the rings seen in this source are not correlated to condensation fronts of carbon monoxide, or any other species with a freeze-out temperature less than 20 K.

4.2 A kinematic excess in the annular gap

A kinematic excess azimuthally spanning a PA range of $\sim 60°$ to $45°$ with a magnitude of $\sim 75$ ms$^{-1}$ is detected in the residual velocities of $^{12}$CO, post-subtraction of a Keplerian model (Fig. 4).

Radially the feature extends between the B1 and B2 dust rings, and at PA of $\sim 43.8°$ is found to overlap well with the high-intensity residual (blob D) reported in Gratton et al. (2019) at a radius of $\sim 38$ au; represented as a green circle in Fig. 4. Counterparts of this feature at lower disc altitudes ($^{13}$CO and C$^{18}$O residual velocity maps; Fig. 5) are found to be near absent however. This may be due to either (1) insufficient integration time of the fainter tracers to resolve a low magnitude velocity deviation, or (2) a variation in the gas rotation profile between the three tracers such that any deviations in the vertical velocity component are near absent for the mid-plane tracers.

A break down of the $^{12}$CO velocity residuals into the $v_\phi$, $v_r$, and the $v_a$ components (Fig. 9) reveal velocity perturbations with magnitudes of $\sim 50$, $40$, and $20$ ms$^{-1}$, respectively. The extraction of the three velocity components is performed on azimuthally averaged velocity residuals, hence the magnitude of the perturbations are lower than the maximum deviations seen in the 2D velocity residual maps. We also extract velocity profiles for a further degraded beam of 0.15 arcsec (overlaid in Fig. 9), and find that the general profile of the velocity residuals at this resolution remains consistent with those extracted at the 0.1 arcsec resolution, suggesting that sub-beam intensity gradients do not play a significant role in the extracted rotation curves.

4.3 Background velocity deviations from the pressure gradient

In EDDY we subtract both a Keplerian only model and a tapered Keplerian model where the latter better mimics the slowed gas rotational profile in the outer regions ($> 100$ au). However, from Figs 1 and 2 it is evident that even interior to 100 au the disc harbours multiple localized pressure gradients associ-
ated with the concentric rings seen in both dust and gas emission.

In Fig. 7, we use the azimuthally averaged gas surface density profile to compute the global gas rotational velocity profile for a pressure-supported disc (for both the upper and lower bounds of the gas density profile). We show the velocity deviations introduced from the localized pressure gradients in the right panel. We also overlay these perturbations with those from a more degraded beam (≈0.1 arcsec) to match the angular resolution of the line maps used in EDDY. For a 0.1 arcsec beam, the kinematic deviation from the pressure gradient is approximately 10 ms$^{-1}$ between the G1 gap and B2 dust ring. Including the self-gravity term from equation (1) is found to have negligible effect on the background velocity perturbations (difference of ≈0.25 ms$^{-1}$ at 100 au).

In Fig. 8, we use the continuum-subtracted azimuthally averaged pressure gradient profile along with a Keplerian profile to compute a fully pressure-supported background disc model. This model is then subtracted from the line-of-sight $^{12}$CO map (Fig. 4). The shape of the arc is found to be identical between the residual velocity maps post-subtraction of a Keplerian-only model and a pressure-supported gas rotational velocity model. The magnitude of the offset is however found to be slightly lower at ≈60–70 ms$^{-1}$. This demonstrates that the $^{12}$CO kinematic arc is in excess of deviations introduced from local pressure gradients in the disc.

4.4 Planetary mass estimate

One possibility for velocity perturbations of the order of a few 10s of ms$^{-1}$ magnitude may be attributed to embedded planet(s). Given that an embedded planet would carve a gap via the exchange of angular momentum with the neighbouring fluid as a result of the tidal torque induced on to the planet by the wake. If the counter-balancing viscous torque is much lower than the rate of angular momentum exchange.
between the planet and neighbouring fluid, then a prominent gaplike structure is created. Therefore, the gap width and depth from observations can be directly used to infer the mass of the planetary body responsible for carving the gap (Kanagawa et al. 2015; Dong & Fung 2017). The relation between gap depth, planet-to-star mass ratio, and disc properties is given by (Kanagawa et al. 2015),

$$\frac{\Sigma_0}{\Sigma_{gap}} - 1 = 0.043 \left( \frac{M_p}{M_*} \right)^2 \left( \frac{h}{r} \right)^{-5} \alpha^{-1},$$

(9)

where $\Sigma_{gap}$ and $\Sigma_0$ are the gas surface densities with and without depletion due to an embedded planet. $M_p$ and $M_*$ are the planet and stellar masses, respectively, $\alpha$ is the disc viscosity. $h/r$ is the disc aspect ratio where the hydrostatic scale height ($h$) is given by equation (5).

Using $^{13}$CO as a temperature proxy within the G1 gap (at $r \approx 38$ au), a hydrostatic scale height of $\sim 2.95$ au is found for a temperature of 58 K and stellar mass of 1.48$M_\odot$, giving a $h/r$ of $\sim 0.08$. From panel (a) in Fig. 7, $\Sigma_0$ and $\Sigma_{gap}$ are estimated to be $\sim 0.75$ and 0.1 g cm$^{-2}$ at $r \approx 38$ au, respectively. These measurements give an estimated planet mass of $\sim 1 M_J$, for a disc viscosity ($\alpha$) of $10^{-3}$ (e.g. Mulders & Dominik 2012; Ansdell et al. 2018). This estimate of the planetary mass using the gas profile is comparable to the estimates made using dust emission in Dong & Fung (2017) for the same disc viscosity and aspect ratio. Equivalently, this also translates to a thermal mass (Goodman & Rafikov 2001),

$$m_\text{th} = \frac{2}{3} \left( \frac{h_0}{r_p} \right)^3 M_*,$$

(10)

of approximately 0.48$M_J$, equivalent to half the planet mass. Estimated planetary masses are sensitive to variation in the thermal structure of the disc (refer to equation 9). Hence, the analytics instead use thermal mass to estimate expected velocity perturbations without requiring a good constraint on the thermal structure.

Figure 5. Same as Fig. 4 but for $^{13}$CO and C$^{18}$O. Top panel: $^{13}$CO. Bottom panel: C$^{18}$O. First column: line-of-sight velocity map. Second column: residual velocity maps post-subtraction of a Keplerian disc model. Third column: residual velocity maps post-subtraction of a tapered Keplerian model. Fourth column: residual velocities in the third column divided by the statistical uncertainty in the line-of-sight velocity maps. The grey shaded area represents the masked-out regions in the MCMC fitting. The dotted rings represent the G1[38au] gap and B2[59au] dust ring, overlaid for comparison. The green circle marks the location of the high-intensity point source (blob D) reported in Gratton et al. (2019).

Figure 6. Gas column density maps computed for when excluding (a) and including (b) the effects of continuum subtraction on line emission. Beam is presented in the bottom-left corner. Both maps are deprojected for a disc inclination of 13° along a PA of 95°.
4.5 Comparison of the super-Keplerian arc to semi-analytical wake models

In Section 4.4, we deduced a planet mass of 1 M_J. Comparison plot of wake models in Fig. 10 demonstrates that a coplanar 1 M_J embedded body does not reproduce a signature large enough to explain the \( \sim 75 \text{ m s}^{-1} \) velocity deviations seen in the observations. Instead, from free exploration of the parameter space, we find kinematic deviations from a 10 M_J mass planet are more consistent with the observations. This qualitative discrepancy in planet mass is likely the result of the near pole-on orientation of the disc. At an inclination of 13°, the projected velocities in the observations may be dominated by the vertical velocity component, while the semi-analytic models only consider deviations in the plane of the disc (\( v_z = 0 \)), thus overpredicting planetary masses. In this scenario, 10 M_J serves as an upper limit rather than a proxy for the true planet mass.

Ligi et al. (2018) and Gratton et al. (2019) have suggested clockwise rotation for the disc to be more consistent with the observed location of the point-like sources across time as detected in high-contrast imaging. This is in agreement with our observations of the \(^{12}\text{CO} \) velocity fields (Fig. 4), where the high-velocity contours are found to slightly bend towards the West side of the minor axis. In comparison, we find the outer wake for a planet in prograde rotation to the disc (clockwise) extends in the opposite direction to the \(^{12}\text{CO} \) arc, and instead more closely resembles a Doppler-flip (Casassus & Pérez 2019) rather than an extended arc-like structure. While unlikely, we also consider retrograde motion. In this scenario, the orientation of the outer wake is found to be more in line with the
Figure 9. Velocity components. Row 1: azimuthally averaged gas rotational velocity \( v_\phi \) for each tracer. Rows 2–4: profiles of the component velocities extracted from the velocity residual maps shown in Figs 4 and 5: rotational (\( v_\phi - v_\text{mod} \)), radial (\( v_\text{rad} \)), and vertical (\( v_z \)), respectively. For the Keplerian profiles a stellar mass of 1.48\( M_\odot \) is used. Velocity profiles for a further degraded beam of 0.15 arcsec are also overlaid.

5 DISCUSSION

5.1 Potential origins for the kinematic residual

5.1.1 Is there an embedded planet in the gap?

The relative depletion in the gas surface density profile infers a planetary mass of 1\( M_\oplus \), consistent with planet mass estimates derived using dust emission (Dong & Fung 2017; Bae et al. 2018; Lodato et al. 2019). However, a few caveats that still remain are:

(i) uncertainty on the gas surface density profile. Ambiguity on the level of self-absorption between dust and gas emission in the disc results in an order-of-magnitude uncertainty on the gas surface density profile computed with and without continuum subtraction. Additionally, the use of molecular line emission relies on a scaling ratio between the molecular species used and \( H_2 \), which here has been pre-defined to equal ISM estimates. In planet-forming discs several processes (isotope-selective photodissociation, freeze-out, and fractionation reactions) have been shown to drive relative isotopic ratios away from ISM estimates (Miotello, Bruderer & van Dishoeck 2014). Collectively, these factors result in an order-of-magnitude uncertainty in the derived planetary mass from equation (9) for a fixed disc aspect ratio and viscosity.

(ii) uncertainty on the disc thermal structure and viscosity. Planet mass estimates from equation (9) are sensitive to variations in the disc aspect ratio. To derive a planet mass of 10\( M_\oplus \) using the current gas surface density profile requires either an increase in the disc aspect ratio by a factor of \( \sim 2.5 \) (hr \( \sim 0.2 \)) or a disc viscosity of \( 10^{-1} \). We can safely rule out a disc aspect ratio of 0.2 as a potential scenario, as this would in turn require a brightness temperature of \( \sim 400 \) K at an orbital radius of \( \sim 38 \) au (refer to equation 5). Disc viscosities in the range \( 10^{-3} – 10^{-2} \) would result in a planet mass range of \( \sim 1–3 \)\( M_\oplus \), comparable to the \( \sim 1–4 \)\( M_\oplus \) estimate made for blob D in Gratton et al. (2019).

(iii) limited spatial resolution. The level of detail in observational data is intrinsically limited by the spatial resolution, spectral reso-
lution, and noise. The quality of the data also serves as a caveat in interpreting kinematic signatures. The effects of beam smearing have been suggested to produce artificial kinematic signatures (Kepler et al. 2019; Boehler et al. 2021). This effect is noted to be the most prominent across regions of a map with steep brightness gradients. The arc in $^{12}$CO spans a region of the map that does not exhibit steep azimuthal variation in brightness. Thus, ruling out any significant contamination by beam smearing in this scenario. However, to fully characterize the kinematic signature in $^{12}$CO, we suggest re-observing HD 169142 at a higher spatial resolution ($<1/3$ the gap) and longer integration times (to achieve an SNR > 8 at the location of the super-Keplerian arc).

5.1.2 Misaligned discs?

Near-IR polarized intensity images of HD 169142 show signatures of shadowing across the outer composite dust rings along the major axis (Quanz et al. 2013; Pohl et al. 2017; Bertrang et al. 2018; Rich et al. 2022). One explanation for such shadows is subdivision and misalignment of the disc. Theoretical work by Young et al. (2022) demonstrate that subtraction of Keplerian models with a constant PA and inclination used throughout the disc can give rise to spurious spiral arms and/or central warps. In particular, their study produces multiple large arc-like features extending across a wide PA range, reminiscent of the kinematic excess observed in $^{12}$CO. Given the disagreement between the wake models to the observations, we propose disc misalignment as a plausible origin to the velocity residuals in Fig. 4; however a full parameter space analysis is beyond the scope of this paper.

5.2 Is there a binary in the central cavity?

Several propositions have been made as to the origin of the central cavity first seen in dust emission in Honda et al. (2012), Osorio et al. (2014), and Fedele et al. (2017). Theoretical work by Toci et al. (2020) demonstrated that a few Jupiter-mass planet placed close to the inner edge of the B1 dust ring could replicate a central cavity of a comparable size to the observations. Independently, Poblete et al. (2022) demonstrated that a stellar binary with a companion mass ratio of 0.1, semimajor axis 9.9 au, and eccentricity of 0.2, oriented at a 90° inclination (polar) to the plane of the disc, could reproduce not only a comparable cavity size but also the azimuthally uneven distribution of dust emission at mm-wavelengths for the B1 ring.

As shown in Section 4.1, a central gas-depleted cavity is present in all three gas tracers, including the optically thick $^{12}$CO $J = 2-1$ emission. While small-scale velocity perturbations are observed in the range $\sim50$–$75$ ms$^{-1}$ in magnitude, the line-of-sight velocity maps (refer to Fig. 4) show no large-scale perturbations. Globally, the disc is found to be in near-Keplerian orbit.

We compare the line-of-sight velocity fields from the proposed polar binary hydrodynamical model in Poblete et al. (2022) with our observations (Fig. 11). Two instances of the polar binary model are used, one with a longitude of the ascending node ($\Omega$) of 0° and another with 90°. Both set of models are processed through MCFOST and convolved to a spatial and spectral resolutions of 0.1 arcsec and 167 ms$^{-1}$ respectively, to match the observations. The MCFOST products are then processed through BETTERMOMENTS to produce line-of-sight velocity maps using the Gaussian method.

Velocity fields from the current polar binary configuration show a central warp in the kinematics (Fig. 11; in conflict with the observations). This suggests that either (i) the stellar mass companion ratio ($0.1 \times M_{\text{primary}}$) is too large; (ii) the current binary orientation induces greater velocity perturbations in the vertical direction than necessary; or (iii) the gas-density depletion in the central cavity is not due to a stellar binary.

6 CONCLUSION

Our analysis of the ALMA band 6 observations of the disc around HD 169142:
Figure 11. A warp in the velocity fields of a polar binary model. Left and middle panels: synthetic velocity fields maps of the polar binary model presented in Poblete et al. (2022) with an Ω of 0° and 90°, respectively. Right panel: velocity fields map of the 12CO line emission shown in Fig. 4, top left panel.

(i) shows a central gas-depleted cavity (R_{cav} ~ 22 au) and annular gap (~38 au). This is accompanied by two concentric gas rings seen in all three (12CO, 13CO, and C18O J = 2-1) tracers (Fig. 1). The brightness temperature profile of all three tracers (including the optically thin tracer, C18O) are found to remain above the CO freeze-out temperature of ~20 K within the inner 200 au. Even at low disc altitudes, temperatures above sublimation favour a dynamical origin to the morphology of the gas structure, rather than a chemical one (Fig. 3).

(ii) finds a super-Keplerian kinematic excess azimuthally spanning across a PA range of −60° to 45° and radially in between the B1[26au] and B2[59au] dust rings (Fig. 4), resembling an arch-like structure. This velocity deviation is found to be in excess of background perturbations from localized pressure gradients and self-gravity (Fig. 8). Part of this feature is found to closely overlap with the location of a high-intensity blob reported in Gratton et al. (2019). Analytical models of planet–disc interaction do not appear to reproduce the observed kinematics, suggesting that if they are caused by a planet, the planet must be on an inclined orbit.

(iii) demonstrates that the relative depletion in the gas surface density profile corresponds to a 1 M_J planet (Fig. 6; Section 4.4), consistent with the estimates made using dust emission (Dong & Fung 2017; Bae et al. 2018; Lodato et al. 2019).

(iv) shows relatively smooth kinematics within the central cavity. In comparison, the current polar binary model proposed in Poblete et al. (2022) results in resolved warping of the high-velocity fields (Fig. 11). Therefore, we reconsider this model as being responsible for depleting the gas and dust content in the central cavity.

ACKNOWLEDGEMENTS

HG, CP, IH, and DJP acknowledge funding from the Australian Research Council via grant DP180104235. CP also acknowledges funding from grant FT170100040. JC acknowledges support the LANL LDRD program. Approved for release as LA-UR-22-31256. VC acknowledges support from the Belgian FRIS-FNRS. This paper uses the following ALMA data: ADS/JAO.ALMA#2015.1.00490.S and ADS/JAO.ALMA#2016.1.00344.S. ALMA is a partnership of ESO (representing its member states), NSF (USA), and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/NRAO, and NAOJ. The National Radio Astronomy Observatory is a facility of the National Science Foundation operated under cooperative agreement by Associated Universities, Inc. This paper uses the following publicly available programs: MCFOST, https://github.com/cpinte/mcfost; PYMCFOST, https://github.com/cpinte/pymcfost; BETTERMOMENTS, https://github.com/richteague/bettermoments; EDDY, https://github.com/richteague/eddy; and WAKEFLOW, https://github.com/TomHilder/wakeflow. The polar binary PHANTOM models were provided by Pedro P. Poblete. Finally, we thank Sebastián Pérez for helpful discussions.

DATA AVAILABILITY

The original raw data sets are publicly available on the ALMA archive under Project codes 2015.1.00490.S and 2016.1.00344.S. The self-calibrated products are available via request from the corresponding author.

REFERENCES

ALMA Partnership, 2015, ApJ, 808, L3
Andrews S. M. et al., 2016, ApJ, 820, L40
Andrews S. M. et al., 2018, ApJ, 869, L41
Ansdell M. et al., 2018, ApJ, 859, 21
Ayliffe B. A., Laibe G., Price D. J., Bate M. R., 2012, MNRAS, 423, 1450
Bae J., Pinilla P., Birnstiel T., 2018, ApJ, 864, L26
Bertrang G. H. M., Avenhaus H., Casassus S., Montesinos M., Kirkchschläger F., Perez S., Cieza L., Wolf S., 2018, MNRAS, 474, 5105
Biller B. A. et al., 2014, ApJ, 792, L22
Blondel P. F. C., Dijie H. R. E. T. A., 2006, A&A, 456, 1045
Boehler Y. et al., 2021, A&A, 650, A59
Bollati F., Lodato G., Price D. J., Pinte C., 2021, MNRAS, 504, 5444
Casassus S., Pérez S., 2019, ApJ, 883, L41
Casassus S. et al., 2021, MNRAS, 507, 3789
Dipierro G., Price D., Laibe G., Hirsh K., Cerioli A., Lodato G., 2015, MNRAS, 453, L73
Dong R., Fung J., 2017, ApJ, 835, 146
Dong R., Fung J., Chiang E., 2016, ApJ, 826, 75
Dunkin S. K., Barlow M. J., Ryan S. G., 1997, MNRAS, 286, 604
Fedele D. et al., 2017, A&A, 600, A72

MNRAS 517, 5942–5958 (2022)
APPENDIX A: FORMULAE TO COMPUTE MOLECULAR GAS COLUMN DENSITY

A1 Optical depth

Prior to computing gas column density, the optical depths of the emission lines intended to be used needs to be determined, to ensure an optically thick tracer will be used to trace gas kinematic temperature, while the tracer intended for computing column density is indeed optically thin. Under the assumption of local thermal equilibrium, optical depths (τ) can be roughly estimated using the line ratio R between two tracers close in frequency (e.g. Lyo et al. 2011; Kastner et al. 2018),

\[
R = \frac{\tau_1}{\tau_2} = \frac{1 - e^{-\tau_1}}{1 - e^{-\tau_2}} = \frac{1 - e^{-\tau_1}}{1 - e^{-\tau_1/\lambda}} \tag{A1}
\]

where \(\tau_1, 2\) are the rest frequencies of the lines. \(X\) is the molecular abundance ratio between the two lines.

A2 Molecular column density

The molecular column density (in units of molecules per m²) for an optically thin uniform slab is given by

\[
N_{\text{mol}} = \frac{N_a}{2J + 1} \exp \left( \frac{E_u}{kT_{\text{ex}}} \right) \tag{A2}
\]

where \(J = 2, k\) is the Boltzmann constant, \(E_u\) is the energy of the upper state, and Z is the partition function of a linear molecule.

The population in the upper energy state, \(N_u\), is given by (Mangum & Shirley 2015),

\[
N_u = \frac{4\pi}{h \nu A_{dd}} B_u(T_{\text{ex}}) - B_v(T_{\text{eq}}) \int (I_v - I_{v, bg}) \, dv \tag{A3}
\]

where \(A_{dd}\) is the Einstein coefficient for spontaneous emission, \(h\) is Planck’s constant, \(v\) is the rest frequency, \(T_{\text{ex}}\) is the excitation temperature, \(I_v - I_{v, bg}\) is the specific intensity minus the background, e.g. the quantity directly measured by the interferometer due to spatial filtering, and \(f\) is the beam filling factor, where \(f = 1\) corresponds to the scenario where emission completely fills the beam.

APPENDIX B: CHANNEL MAPS
Figure B1. ALMA data: $^{12}$CO $J = 2-1$ channel maps.

Figure B2. MCFOST synthetic data: $^{12}$CO $J = 2-1$ channel maps with an embedded $10M_J$ planet at 38 au from disc centre.
Figure B3. Residual $^{12}$CO J = 2-1 channel maps: [ALMA data – MCFOST synthetic data]. The grey shaded area represents a mask at $r > 200$ au; the outer radius of our synthetic data in Fig. B2. Here, we stress that non-zero brightness residuals should not be inferred as a proxy for the goodness of fit of the velocity fields.

Figure B4. $^{13}$CO J = 2-1 channel maps.
APPENDIX C: INCORPORATING UNCERTAINTIES TO THE BEST-FITTING PARAMETERS DETERMINED FROM EDDY
Figure C1. **Uncertainty series**: $^{12}$CO residual velocity maps for varying quantities of $M_\odot$, inclination and PA around the best-fitting values determined from the MCMC fitting in EDDY.

This paper has been typeset from a TeX/LaTeX file prepared by the author.