Boosting Spatial Reuse via Multiple Paths Multi-Hop Scheduling for Directional mmWave WPANs

Yong Niu, Chuhan Gao, Yong Li, Member, IEEE, Depeng Jin, Li Su, and Dapeng (Oliver) Wu, Fellow, IEEE

Abstract—With huge unlicensed bandwidth available in most parts of the world, millimeter wave (mmWave) communications in the 60 GHz band has been considered as one of the most promising candidates to support multi-gigabit wireless services. Due to high propagation loss of mmWave channels, beamforming is likely to become adopted as an essential technique. Consequently, transmission in 60 GHz band is inherently directional. Directivity enables concurrent transmissions (spatial reuse), which can be fully exploited to improve network performance. In this paper, we propose a multiple paths multi-hop scheduling scheme, termed MPMH, for mmWave wireless personal area networks, where the traffic across links of low channel quality is transmitted through multiple paths of multiple hops to unleash the potential of spatial reuse. We formulate the problem of multiple paths multi-hop scheduling as a mixed integer linear program (MILP), which is generally NP-hard. To enable the implementation of the multiple paths multi-hop transmission in practice, we propose a heuristic scheme including path selection, traffic distribution, and multiple paths multi-hop scheduling to efficiently solve the formulated problem. Extensive simulation results demonstrate MPMH achieves near-optimal network performance in terms of transmission delay and throughput, and enhances the network performance significantly compared with existing protocols.

I. INTRODUCTION

Recently, millimeter wave (mmWave) communications in the 60 GHz band has attracted considerable interest from academia, industry, and standards bodies. Due to its huge unlicensed bandwidth (i.e., up to 7 GHz in the USA), 60 GHz communications is able to support multi-gigabit wireless services, such as high-speed data transfer between devices (e.g., cameras, pads, and personal computers), wireless gigabit ethernet, wireless gaming, and real-time streaming of both the compressed and uncompressed high definition television. Meanwhile, rapid progress in 60-GHz mm-wave circuits, including on-chip and in-package antennas, radio frequency (RF) power amplifiers (PAs), low-noise amplifiers (LNAs), voltage-controlled oscillators (VCOs), mixers, and analog-to-digital converters (ADCs) has accelerated popularization of wireless products and services in the 60 GHz band [1]–[3]. In terms of standardization, several standards have been defined for indoor wireless personal area networks (WPAN) and wireless local area networks (WLAN), for example, ECMA-387 [4], IEEE 802.15.3c [5], and IEEE 802.11ad [6]. Due to high carrier frequency, mmWave communication systems are fundamentally different from other existing communication systems using lower carrier frequencies (e.g., from 900 MHz to 5 GHz). Therefore, network architectures and protocols, especially medium access control (MAC) mechanism, require new thinking to fully unleash the potential of mmWave communications.

MmWave communications in the 60 GHz band suffers from high propagation loss. The free space propagation loss scales as the square of the wavelength, which indicates that the free space propagation loss at 60 GHz band is 28 decibels (dB) more than that at 2.4 GHz [7]. Thus, 60 GHz communications is mainly used for short-range indoor communications. To combat severe channel attenuation, high gain directional antennas are utilized at both the transmitter and receiver, where beamforming has been adopted as an essential technique to search for the best antenna weight vectors (AWV) [8]–[10].

With directional transmission, the third party nodes cannot perform carrier sense as in IEEE 802.11 to avoid contention with current transmission, which is known as the deafness problem [11]. On the other hand, there is less interference between links, and thus concurrent transmission (spatial reuse) can be exploited to greatly increase the network capacity. However, on one hand, for flows across links of low channel quality or with significantly higher traffic demand, more network resources (e.g., time slots) are needed. In this case, these extra resources cannot be utilized efficiently due to less spatial reuse. Consequently, system performance is degraded significantly. Thus, more efficient transmission mechanisms are needed to address the performance degradation when there are flows across links of low channel quality or with significantly higher traffic demand. For example, in [12], a traffic flow of a long hop is transmitted over multiple short hops to improve flow throughput. Similarly, in D-CoopMAC [13], the direct long link is replaced by a two-hop link if a relay that has higher rate links with both source and destination exists. On the other hand, for flows supporting applications of...
high throughput, such as high-definition television (HDTV), much more time slots are needed to satisfy their throughput requirements in TDMA-based protocols such as IEEE 802.15.3c. Consequently, there are not enough time slots allocated for other flows, which may lead to serious unfairness in WPANs. Besides, the number of flows scheduled each time in these protocols will be very small. Therefore, fully exploiting spatial reuse to improve the throughput of these flows while achieving high system performance is an important and challenging issue.

Recently, the hybrid beamforming structure has been proposed to obtain the multiplexing gain of Multiple-Input Multiple-Output (MIMO) and also provide high beamforming to overcome high propagation loss in mmWave bands [14]. In the hybrid beamforming structure, multiple RF links can be established via the design of the digital precoder and the analog beamformer to reap the spatial multiplexing gain of MIMO [15]. To improve the throughput of flows of low channel quality or with high traffic demand, transmitting these flows through multiple paths concurrently similar to the multiple RF links in the hybrid beamforming structure will be an effective way, and should be considered in the design of scheduling schemes for mmWave communications.

In this paper, motivated by the spatial multiplexing structure in hybrid beamforming, we propose a novel multiple paths multi-hop scheduling scheme (MPMH) to boost the spatial reuse in mmWave WPANs. By transmitting the traffic of flows with low channel quality on the direct paths or high traffic demand through multiple paths concurrently similar to the multiple RF links in the hybrid beamforming structure will be an effective way, and should be considered in the design of scheduling schemes for mmWave communications.

This paper is organized as follows. We discuss related work on concurrent transmission scheduling for mmWave WPANs in section II. In section III, we present the system model and illustrate our basic idea by an example. We formulate the optimal multiple paths multi-hop scheduling problem as an MILP in section IV. The MPMH scheme is illustrated in section V. In section VI, we evaluate the performance of MPMH under various traffic patterns and simulation parameters. Finally, we conclude this paper in section VII.

II. RELATED WORK

Transmission scheduling for mmWave communications in the 60 GHz band has been investigated in the literature [11], [13], [17], [20], [22], [27]. Since ECMA-387 [11] and IEEE 802.15.3c [5] adopted time division multiple access (TDMA), some work is also based on TDMA [17]. [18], [22], [23], [26], [27]. In two protocols based on IEEE 802.15.3c, multiple links are scheduled to communicate in the same slot if the multi-user interference (MUI) is below a specific threshold [17], [18]. Cai et al. [22] introduced the concept of exclusive region (ER) to enable concurrent transmissions, and derived the ER conditions that concurrent transmissions always outperform TDMA. Qiao et al. [23] proposed a concurrent transmission scheduling algorithm for an indoor IEEE 802.15.3c WPAN, where non-interfering and interfering links are scheduled to transmit concurrently to maximize the number of flows with the quality of service requirement of each flow satisfied. Furthermore, multi-hop concurrent transmissions (MHCT) are enabled to address the link outage problem (blockage) and to combat huge path loss to improve flow throughput [12]. MHCT, however, only transmits traffic of flows through multiple hops on one path, and does not exploit the concurrent transmissions on multiple paths to improve flow throughput and network throughput. In IEEE 802.15.3c, during the random access period, the piconet controller is in the omni-directional mode to solve the deafness problem, which may not be feasible for mmWave systems of the multi-gigabit domain with highly directional transmissions. For bursty traffic patterns such as the Interrupted Poisson Process (IPP), TDMA based protocols may result in over-allocated medium access time for some users while resulting in under-allocated medium access time for others.

There is some other work based on a central controller to coordinate the transmissions in WPANs [11], [13], [19], [20], [24]. Gong et al. [19] proposed a directional carrier sense multiple access with collision avoidance (CSMA/CA) protocol, which mainly focuses on solving the deafness problem. It exploits virtual carrier sensing, and depends on the piconet coordinator (PNC) to distribute the network allocation vector (NAV) information. However, it does not exploit the spatial reuse fully and also does not consider multiple paths multi-hop transmissions. In the multi-hop relay directional MAC protocol (MRDMAC), if a wireless terminal (WT) is lost, the access point (AP) will choose a WT among the live WTs to act as a relay to the lost node [20]. However, MRDMAC does not fully exploit spatial reuse since most transmissions go through the piconet coordinator (PNC). Chen et al. [24] proposed a spatial reuse strategy to schedule two different service periods (SPs) to overlap with each other.
for an IEEE 802.11 ad WPAN. Recently, Son et al. \[11\] proposed a frame based directional MAC protocol (FDMAC). The high efficiency of FDMAC is achieved by amortizing the scheduling overhead over multiple concurrent transmissions in a row. The core of FDMAC is the Greedy Coloring algorithm, which fully exploits spatial reuse and greatly improves the network throughput compared with MRDMAC \[20\] and memory-guided directional MAC (MDMAC) \[21\]. FDMAC also has a good fairness performance and low complexity. FDMAC, however, does not consider multiple paths multi-hop transmission to improve flow throughput of links with poor quality. Chen et al. \[13\] proposed a directional cooperative MAC protocol, termed D-CoopMAC, to coordinate the uplink channel access among stations in an IEEE 802.11ad WLAN. In D-CoopMAC, the multirate capability of links is exploited to select a relay station for the direct link; when the two-hop link outperforms the direct link, the latter will be replaced by the former. In D-CoopMAC, however, spatial reuse is not considered since most transmissions go through the access point (AP). Most of the above work ignores the negative effect of links with poor channel quality on network performance, such as delay, throughput, and the number of flows scheduled each time. The work above does not boost the potential of spatial reuse via multiple paths multi-hop transmissions.

There is also some related work on maximum independent set and protocol model based scheduling. For protocol model based scheduling, interference is modeled as an interference graph, where each vertex represents a link in the wireless network \[28\]–\[30\]. Two vertices form an edge if these two links cannot be scheduled for concurrent transmissions. This simple interference model does not take the unique features of mmWave links, e.g., directivity, into consideration. Xu et al. \[51\] proposed a constant approximation algorithm for one-slot link scheduling in arbitrary networks under the SINR interference model, where a transmission is successful if the received SINR is more than some threshold. However, it does not consider the directivity of mmWave links, and the interference is only related to the distance between nodes in a two-dimensional Euclidean space. This lack of consideration is unreasonable for mmWave WPANs, especially since the SINR thresholds for all links were kept the same. To the best of our knowledge, we are the first to exploit multiple paths multi-hop transmissions for boosting the spatial reuse gain under the SINR interference model.

### III. System Overview

#### A. System Model

We consider a typical indoor WPAN system composed of several wireless nodes (WNs) and a single piconet controller (PNC) \[5\]. The PNC synchronizes the clocks of other nodes and schedules the medium access of all the nodes to accommodate their traffic demands. The WNs and PNC have electronically steerable directional antennas to support directional transmissions between WNs or between the WN and the PNC by beamforming. The system is partitioned into non-overlapping time slots of equal length, and runs a bootstrapping program \[32\], by which each device knows the up-to-date network topology and the location information of other devices. With this information, the beamforming between nodes can be completed in a short time, and each node can direct its antenna towards other nodes.

We assume there are \(V\) flows with traffic transmission demand in the network. For flow \(v\), we denote its traffic demand as \(d_v\), and numerically \(d_v\) is equal to the number of packets to be transmitted. For 60 GHz wireless channels, non-line-of-sight (NLOS) transmissions suffer from higher attenuation than line-of-sight (LOS) transmissions \[33\], \[34\]. In Ref. \[33\], the path loss exponent in the LOS hall is 2.17, while the path loss exponent in the NLOS hall is 3.01. Thus, if the distance between the transmitter and the receiver is 10 m, the gap between the path loss of LOS hall and NLOS hall is about 10 dB. In a power-limited regime, a 10 dB power loss requires a 10-fold reduction of transmission rate to maintain the same reliability. On the other hand, NLOS transmission in the 60 GHz band also suffers from a shortage of multipath, and restricting to the LOS path can maximize the power efficiency since the LOS path is strongest \[20\]. To achieve high data rate transmission and maximize the power efficiency, we consider the directional LOS transmission case in this paper. For each directional link \(i\), we denote its sender and receiver as \(s_i\) and \(r_i\) respectively. Then according to the path loss model \[23\], the received signal power, denoted by \(P_r\) (mW), can be calculated as

\[
P_r = k_0 P_t l_{s_i,r_i}^{-\gamma},
\]

where \(P_t\) (mW) is the transmission power, \(k_0 = 10^{10P_L/d_0}/10\) is the constant scaling factor corresponding to the reference path loss \(P_L(d_0)\) (dB) with \(d_0\) equal to 1 m, \(l_{s_i,r_i}\) (m) is the distance between node \(s_i\) and node \(r_i\), and \(\gamma\) is the path loss exponent \[23\]. In this paper, we assume fixed transmission power.

We denote the transmission rate of the direct link of flow \(v\) as \(c_v\), and numerically \(c_v\) is equal to the number of packets the link can transmit in one time slot. The transmission rates of links are obtained by a channel transmission rate measurement procedure \[35\]. In this procedure, the sender of each flow transmits measurement packets to the receiver first. After measuring the signal to noise ratio (SNR) of these packets, the receiver obtains the achievable transmission rate, and appropriate modulation and coding scheme (MCS) by the correspondence table about the SNR and MCS. Under low user mobility, the procedure is usually executed, and the transmission rates of links are updated periodically.

Directional transmissions enable less interference between links, and concurrent transmissions of links can be supported to improve network capacity. Due to the limited range for mmWave WPANs, the interference between links cannot be neglected \[22\]. Thus, we adopt the SINR model for concurrent transmission \[24\], \[31\]. For link \(i\) and link \(j\), the received power from \(s_i\) to \(r_j\) can be calculated as

\[
P_{r}^{i,j} = f_{s_i,r_j} k_0 P_t l_{s_i,r_j}^{-\gamma},
\]

where \(f_{s_i,r_j}\) indicates whether \(s_i\) and \(r_j\) direct their beams towards each other. If \(s_i\) and \(r_j\) direct their beams towards each other, \(f_{s_i,r_j} = 1\); otherwise, \(f_{s_i,r_j} = 0\). Then, the received
links in the third pairing are enabled to improve the efficiency of transmission significantly.

IV. Problem Formulation

In this section, we formulate the problem of optimal multiple paths multi-hop scheduling into a mixed integer linear program (MILP) based on the problem formulation in FDMAC [11].

A. Problem Formulation and Analysis

From traffic demand polling, we assume there are $V$ flows to be scheduled by the PNC. For flows across links with a low transmission rate or with a high traffic demand, more time slots are needed to accommodate their traffic demand. Consequently, these extra time slots cannot be used for spatial reuse, which degrades system performance significantly. Thus, flows with lower transmission rate on the direct paths or with higher traffic demand have higher priority to be transmitted through multiple paths for better utilization of spatial reuse. In the following, we propose a criterion to decide whether a flow needs to be transmitted through multiple paths.

For each flow $v$, we define its traffic demand intensity as arrived traffic demand averaged over a relatively long time, which is denoted by $D_{v}$. The transmission rate of its direct path is denoted by $c_{v}$. Then if flow $v$ satisfies

$$\frac{c_{v}}{D_{v}} \frac{\text{avg}(c_{u}, D_{u})}{\epsilon} < 1,$$

then traffic of flow $v$ will be transmitted through multiple paths. $\epsilon$ is defined to control the number of flows transmitted through multiple paths. With a larger $\epsilon$, there may be more flows transmitted through multiple paths; otherwise, fewer flows will be transmitted through multiple paths. Specially, if $c_{v}$ is equal to 0, i.e., the direct path of flow $v$ is blocked, flow $v$ will be transmitted through multiple paths.

For the fairness among flows, if there is no multi-path multi-hop transmission, flows across direct paths of low channel quality or with high traffic demand will occupy a large number of time slots exclusively. With multi-path multi-hop transmission enabled, more flows are able to share the time resources more fully by the concurrent transmissions (spatial reuse). Thus, the fairness performance without multi-path multi-hop transmission will be worse than that with multi-path multi-hop transmission. Therefore, our scheme improves the fairness among flows by the multi-path multi-hop transmission.

We denote the number of paths of the $v^{th}$ flow as $M_{v}$. We also define the number of hops of the $p^{th}$ path of flow $v$ as $H_{vp}$. For flow $v$, the traffic demand distributed to the $p^{th}$ path is denoted as $\alpha_{vp}$. We denote the $i^{th}$ hop link of the $p^{th}$ path of flow $v$ as $(v, p, i)$, and its transmission rate by $c_{vpi}$. For link $(v, p, i)$ and $(u, q, j)$, we define an indicator variable $I_{vpi, uqj}$. $I_{vpi, uqj}$ is equal to 1 if $(v, p, i)$ and $(u, q, j)$ are adjacent, i.e., have common vertices; otherwise, $I_{vpi, uqj}$ is equal to 0.

If there are $K$ pairings in the schedule to accommodate the traffic demand of flows, we denote the number of time slots of the $k^{th}$ pairing as $\delta^{k}$. We also define $\alpha_{vpk}$ to indicate...
whether link \((v, p, i)\) is scheduled in the \(k^{th}\) pairing. If link \((v, p, i)\) is scheduled in the \(k^{th}\) pairing, \(a_{vpi}^k\) is equal to 1; otherwise, \(a_{vpi}^k\) is equal to 0. To optimize system performance, the traffic demand of flows should be cleared in the shortest time [11]. Thus, the problem of optimal multiple paths multi-hop scheduling (P1) is formulated as follows.

\[
\min \sum_{k=1}^{K} \delta^k
\]

\[
s.t.
\]

\[
\sum_{k=1}^{K} a_{vpi}^k \begin{cases} = 1, & \text{if } d_{vp} > 0 \land i \leq H_{vp}, \forall v, p, i \\ = 0, & \text{otherwise;} \end{cases} 
\]

\[
a_{vpi}^k \in \{0, 1\}, \text{ if } d_{vp} > 0 \land i \leq H_{vp}, \forall v, p, i, k
\]

\[
\sum_{k=1}^{K} (\delta^k \cdot a_{vpi}^k) \geq \left\lfloor \frac{d_{vp}}{H_{vp}} \right\rfloor, \text{ if } d_{vp} > 0 \land i \leq H_{vp}, \forall v, p, i
\]

\[
= 0, \text{ otherwise;}
\]

\[
\sum_{p=1}^{M_v} d_{vp} = d_v; \forall v
\]

\[
\sum_{i=1}^{H_{vp}} a_{vpi}^k \leq 1; \forall v, p, k
\]

\[
a_{vpi}^k + a_{uqj}^k \leq 1; \text{ if } I_{vpi, uqj} = 1;
\]

\[
\text{for all } k, \text{ any two links } (v, p, i), (u, q, j)
\]

These constraints are explained as follows.

- Constraint (6) indicates for each link \((v, p, i)\), if there is traffic distributed to it, then it should be scheduled once in one pairing of the frame.
- Constraint (7) indicates for each link \((v, p, i)\), if there is traffic distributed to it, then \(a_{vpi}^k\) is a binary variable; otherwise, \(a_{vpi}^k\) is equal to 0.
- Constraint (8) indicates for each link \((v, p, i)\), if there is traffic distributed to it, then this traffic should be accommodated in the frame.
- Constraint (9) indicates for flow \(v\), the sum of traffic distributed in all paths should be equal to its traffic \(d_v\).
- Constraint (10) indicates links in the same path cannot be scheduled in the same pairing due to the inherent order of transmission in each path. Preceding hops should be scheduled ahead of hops behind on the path since nodes behind on the path are able to relay the packets after receiving the packets from preceding nodes.
- Constraint (11) indicates due to the half-duplex assumption, adjacent links cannot be scheduled in the same pairing.
- Constraint (12) indicates due to the inherent order of transmission in each path, the \(i^{th}\) hop link of the \(p^{th}\) path of flow \(v\) should be scheduled ahead of the \((i + 1)^{th}\) hop link. Constraint (12) represents a group of constraints since \(K^*\) varies from 1 to \(K\).
- Constraint (13) indicates to enable concurrent transmissions, the SINR of each link in the same pairing should be able to support its transmission rate.

\[K^* \sum_{k=1}^{K^*} a_{vpi}^k \geq \sum_{k=1}^{K} a_{vpi(k+1)}^k, \text{ if } H_{vp} > 1;
\]

\[
\forall v, p, i = 1 \sim (H_{vp} - 1), K^* = 1 \sim K
\]

\[W N_0 + \rho \sum_{u=1}^{M_u} \sum_{q=1}^{M_q} \sum_{j=1}^{M_j} J_{uqj}, a_{uqj}^k, k_0 P_i l_{r_{uqj}}^{-\gamma}, r_{vpi}^k \geq M S(v_{pi}) \times a_{vpi}^k, \forall v, p, i, k
\]

B. Problem Reformulation

We can observe that in the constraints (6), (7), and (8) of problem (P1), the condition “if \(d_{vp} > 0\)” has the variable \(d_{vp}\). This problem form is intractable. If we select the paths for each flow that needs multiple paths multi-hop transmission by a heuristic path selection algorithm, these paths will have traffic, and their conditions “if \(d_{vp} > 0\)” will be met. In this case, we can remove “if \(d_{vp} > 0\)” from constraints (6), (7), and (8), and problem (P1) becomes a mixed integer nonlinear program (MINLP). However, it is still difficult to obtain the optimal solution since constraints (8) and (13) are nonlinear.
If the nonlinear terms of problem (P1) can be linearized, problem (P1) will become a standard mixed integer linear program (MILP), which can be solved by some existing sophisticated algorithms, such as the branch-and-bound method [86]. For the second order terms in constraints (8) and (13), we adopt a relaxation technique, the Reformulation-Linearization Technique (RLT) [11], [36] to linearize constraints (8) and (13). The RLT technique produces tight linear programming relaxations for an underlying nonlinear and non-convex polynomial programming problem. In the procedure, a variable substitution is applied for each nonlinear term to linearize the objective function and the constraints of this problem. Besides, nonlinear implied constraints for each substitution variable are generated by taking the products of bounding terms of the decision variables, up to a suitable order. Specially, we present the RLT procedures for (8) and (13) in the following.

For constraint (8), we define a substitution variable \( s_{vpi}^k = \delta^k \cdot a_{vpi}^k \). Since the traffic of one link should be accommodated in one pairing, the number of time slots of each pairing, \( \delta^k \) is bounded as \( 0 \leq \delta^k \leq \bar{d} \), where \( \bar{d} = \max (\{ \frac{d_{uqj}}{a_{vpi}} \} \text{ for all } v, p, i) \). We also know \( 0 \leq a_{vpi}^k \leq 1 \). Then we can obtain the RLT bound-factor product constraints for \( s_{vpi}^k \) as

\[
\begin{align*}
\{ [\delta^k - 0] \cdot [a_{vpi}^k - 0] \} & \geq 0 \\
\{ [\bar{d} - \delta^k] \cdot [a_{vpi}^k - 0] \} & \geq 0 \\
\{ [\delta^k - 0] \cdot [1 - a_{vpi}^k] \} & \geq 0 \\
\{ [\bar{d} - \delta^k] \cdot [1 - a_{vpi}^k] \} & \geq 0
\end{align*}
\]

\{LS\} represents a linearization step under \( s_{vpi}^k = \delta^k \cdot a_{vpi}^k \). By substituting \( s_{vpi}^k = \delta^k \cdot a_{vpi}^k \), we obtain

\[
\begin{align*}
& s_{vpi}^k \geq 0 \\
& \bar{d} \cdot a_{vpi}^k - s_{vpi}^k \geq 0 & \text{for all } v, p, i, k. \\
& \delta^k - s_{vpi}^k \geq 0 \\
& \bar{d} - \delta^k - \bar{d} \cdot a_{vpi}^k + s_{vpi}^k \geq 0
\end{align*}
\]

For constraint (13), we first convert it to

\[
(k_0 P_{ls_{vpi},vpi}^{-\gamma} - MS(c_{vpi}) W N_0) a_{vpi}^k \geq \sum_{u=1}^{V} \sum_{q=1}^{M_u} \sum_{j=1}^{H_uq} f_{s_{uqj},vpi} a_{vpi}^k a_{uqj}^k P_{ls_{uqj},vpi}^{-\gamma}
\]

\[
MS(c_{vpi}) P_{ls_{vpi},vpi}^{-\gamma} - MS(c_{vpi}) W N_0) a_{vpi}^k \geq \sum_{u=1}^{V} \sum_{q=1}^{M_u} \sum_{j=1}^{H_uq} f_{s_{uqj},vpi} a_{vpi}^k a_{uqj}^k P_{ls_{uqj},vpi}^{-\gamma}
\]

For the second order term \( a_{vpi}^k a_{uqj}^k \), we define \( \omega^k_{vpi,uqj} = a_{vpi}^k a_{uqj}^k \) as the substitution variable. Since \( 0 \leq a_{vpi}^k \leq 1 \) and \( 0 \leq a_{uqj}^k \leq 1 \), the RLT bound-factor product constraints for \( \omega^k_{vpi,uqj} \) are

\[
\begin{align*}
& \omega^k_{vpi,uqj} \geq 0 \\
& a_{vpi}^k - \omega^k_{vpi,uqj} \geq 0 \\
& a_{uqj}^k - \omega^k_{vpi,uqj} \geq 0 \\
& 1 - a_{vpi}^k - a_{uqj}^k + \omega^k_{vpi,uqj} \geq 0
\end{align*}
\]

After substituting \( s_{vpi}^k \) and \( \omega^k_{vpi,uqj} \) into constraint (8) and constraint (13), we obtain a mixed integer linear program (MILP) relaxation (P2) as

\[
\begin{align*}
\min \sum_{k=1}^{K} & \delta^k \\
\text{s. t.} & \\
K \sum_{k=1}^{K} s_{vpi}^k & \geq \left[ \frac{d_{uqj}}{a_{vpi}} \right] \text{, if } i \leq H_{vp}, \forall v, p, i \quad \text{(19)} \\
& = 0, \text{ otherwise;}
\end{align*}
\]

\[
(k_0 P_{ls_{vpi},vpi}^{-\gamma} - MS(c_{vpi}) W N_0) a_{vpi}^k \geq \sum_{u=1}^{V} \sum_{q=1}^{M_u} \sum_{j=1}^{H_uq} f_{s_{uqj},vpi} a_{vpi}^k a_{uqj}^k P_{ls_{uqj},vpi}^{-\gamma}, \forall v, p, i, k
\]

Constraints (6) and (7) with “if \( d_{uqj} > 0 \)” removed; Constraints (9), (10), (11), (12), (15), and (17).

As an example, we consider the WPAN of six nodes showed in Fig. 1(b). For the flow from A to B with 18 packets, we select three paths, path 1, path 2, and path 3, which have been illustrated in Fig. 1(b). In this example, we assume for any two nonadjacent links, \( (v, p, i) \) and \( (u, q, j) \), \( \sum_{j=1}^{H_uq} f_{s_{uqj},vpi} \) is equal to 0. Then we solve the problem of (P2) using the branch-and-bound method. The traffic distribution scheme is to send 3 packets through path 1, 9 packets through path 2, and 6 packets through path 3. The transmission phase of the schedule has 9 time slots, and is already illustrated in Fig. 1(a). Compared with the single hop transmission scheme, MPMH reduces the number of time slots for transmission by 50%.

The formulated mixed integer linear program (MILP) problem (P2) is NP-hard. The number of decision variables is \( O((VP_{max} H_{max})^2 K) \), and the number of constraints is \( O((VP_{max} H_{max})^2 K) \), where \( P_{max} \) is the maximum number of paths of flows, and \( H_{max} \) is the maximum number of hops of paths. Using the branch-and-bound algorithm to solve this problem will take significantly long computation time, e.g., several minutes for a 5-node network in [11], which is unacceptable for practical mmWave WPANs where the duration of one time slot is only a few microseconds [11]. Therefore, to implement MPMH scheduling in a practical mmWave WPAN, heuristic algorithms with low computational complexity are needed.

V. THE MPMH SCHEME

To solve problem (P2), which boosts the spatial reuse via multiple paths multi-hop transmissions, firstly we should select suitable transmission paths. Then since the traffic distributed on these paths has a big impact on the efficiency of spatial reuse, traffic of each flow should be distributed on its transmission paths efficiently. Finally, transmission scheduling is needed to accommodate the traffic of all flows with a minimum number of time slots by fully exploiting spatial reuse. Following the above ideas, in this section, we propose a multiple paths multi-hop transmission scheme (MPMH), which consists of three heuristic algorithms respectively for the path selection, traffic distribution, and transmission scheduling.
A. Path Selection

We set the maximum number of hops for each selected path, and denote it by $H_{\text{max}}$. The path selection algorithm first finds out all the possible paths from the sender $s_v$ to the receiver $r_v$ with the number of hops less than or equal to $H_{\text{max}}$, denoted by $P_c(v)$. To exploit higher transmission ability of each path, each hop of these paths should have the same or higher channel quality than the direct path of flow $v$. Besides, each path should have no loop. Besides, if $c_v$ is equal to 0, i.e., the direct path of flow $v$ is blocked, flow $v$ will not be transmitted through its direct path. Then the algorithm examines each path in $P_c(v)$ in order of non-increasing lowest transmission rate on each path. The set of selected paths from $P_c(v)$ is denoted by $P_s(v)$. Since the lowest transmission rate on each path determines its transmission ability, we should first select the paths with high transmission ability into $P_s(v)$. Besides, the paths in $P_s(v)$ should have no common hop to avoid degradation of efficiency. To maximize spatial reuse, the hops with the lowest transmission rate in $P_s(v)$ should be nonadjacent to enable concurrent transmissions. Therefore, $|P_s(v)|$ is bounded by $[n/2]$ with a network of $n$ nodes.

We denote the set of flows that will be transmitted through multiple paths as $F_{\text{mpmh}}$, which is selected according to (3). Then, the path selection algorithm should select suitable paths for each flow $F$ in $F_{\text{mpmh}}$. We denote the sender of flow $F$ as $s_v$, and the receiver of flow $v$ as $r_v$. We also denote the first node and the last node of path $p$ as $f_p$ and $l_p$ respectively. For link from $l_p$ to $i$, we denote its transmission rate by $c_{li}$. The set of possible paths from $s_v$ is denoted as $P(v)$, and $P(v)$ is initialized to the vertex of $s_v$. For each path $p$, we denote the lowest transmission rate on it as $c_{pi}$, and the hop with the lowest transmission rate as $h_l(p)$. We denote the set of lowest transmission rate hops of paths in $P_s(v)$ is denoted as $H_l(P_s(v))$.

The pseudo-code of the path selection algorithm is presented in Algorithm 1. Lines 1–18 find out all the possible paths with the number of hops less than or equal to $H_{\text{max}}$, denoted by $P_c(v)$. For each path in $P(v)$, the algorithm extends this path to generate new paths with no loop, as indicated by lines 3–11. In line 5, the new hop extended from $p$ should have a higher or same transmission rate than that of the direct path of flow $v$. After generating new paths from $P(v)$, the old paths in $P(v)$ are removed as in line 10, and $P(v)$ is updated by the new set of paths $P_{\text{new}}$, as in line 12. For each path $p$ in $P(v)$, if its last node is the receiver $r_v$, then this path will be added to $P_s(v)$, and removed from $P(v)$, as indicated by lines 14–16. Lines 19–28 select the eventual set of transmission paths, $P_s(v)$, from $P_s(v)$. The algorithm first obtains the path with the lowest transmission ability, i.e., the lowest transmission rate on each path, as indicated by line 20. If this path has no common hop with the paths already in $P_s(v)$, and the hop on this path with the lowest transmission rate, $h_l(p)$, is not adjacent to the hops in $H_l(P_s(v))$, this path will be selected into $P_s(v)$, as indicated by lines 21–25. This path is removed from $P_c(v)$ in line 26. When there is no path in $P_c(v)$, the algorithm outputs $P_s(v)$.

For the WPAN in Fig. 1(b), with $H_{\text{max}}$ set to 3, the path selection algorithm obtains three paths for flow $A \rightarrow B$, i.e., path 1, path 2, and path 3 already illustrated in Fig. 1(b).

Algorithm 1 The Path Selection Algorithm

Initialization:

$P(v) = \{s_v\}; P_c(v) = \emptyset; P_s(v) = \emptyset; H_l(P_s(v)) = \emptyset; h=0$;

Iteration:

1. while ($|P(v)| > 0$ and $h < H_{\text{max}}$) do
2. $h=h+1; P_{\text{new}} = \emptyset$;
3. for each $p \in P(v)$ do
4. for each node $i$ with link $l_p \rightarrow i$ unblocked do
5. if ($c_{pi} \geq c_v$ and $i$ is not on $p$) then
6. Generate a new path $p^*$ by extending $p$ to $i$;
7. $P_{\text{new}} = P_{\text{new}} \cup p^*$;
8. end if
9. end for
10. $P(v) = P(v) - p$;
11. end for
12. $P(v) = P_{\text{new}}$;
13. for each $p \in P(v)$ do
14. if ($l_p == r_v$) then
15. $P_s(v) = P_s(v) \cup p; P(v) = P(v) - p$;
16. end if
17. end for
18. end while
19. while ($|P_c(v)| > 0$) do
20. Obtain the path with the largest $c_t(p), p \in P_c(v)$;
21. if ($p$ have no common hop with paths in $P_s(v)$) then
22. if ($h_l(p)$ is not adjacent to the hops in $H_l(P_s(v))$) then
23. $P_s(v) = P_s(v) \cup p; H_l(P_s(v)) = H_l(P_s(v)) \cup h_l(p)$;
24. end if
25. end if
26. $P_s(v) = P_s(v) - p$;
27. end while
28. Output $P_s(v)$.

B. Traffic Distribution

With the results of path selection, we propose a traffic distribution algorithm to distribute the traffic of a flow on the selected multiple paths, i.e., the traffic demand of flow $v$ should be distributed on the set of selected paths, $P_s(v)$. Since the link with the lowest transmission rate on a path determines the transmission ability of the path, we should let the links with lowest transmission rates on different paths transmit concurrently as much as possible, and we also need to maximize the utilization of time slots in a pairing by making as many links as possible to transmit concurrently in each time slot of this pairing. Therefore, the traffic distribution algorithm is the proportional distribution of the traffic according to the lowest transmission rate on each path. For example, for the three paths in Fig. 1(b), since the lowest transmission rates of path 1, path 2, and path 3 are 1, 3, and 2 respectively, the
traffic from A to B is distributed on path 1, path 2, and path 3 according to the proportion of 1:3:2.

C. Transmission Scheduling

After path selection and traffic distribution, the transmission scheduling algorithm computes a near-optimal schedule to accommodate the traffic demand of flows. Since any two adjacent links cannot be scheduled concurrently, it can also be inferred that the maximum number of links that can transmit in the same pairing is \( \lfloor n/2 \rfloor \). Links that are scheduled in the same pairing can be represented by a directive graph, which is a matching. If we assign one of \( K \) colors to each pairing, and all the edges in the same pairing have identical color, each hop will have only one of the \( K \) colors since each hop is only scheduled in one pairing of the frame. Therefore, this process can also be modeled as an edge coloring problem, and the only difference is that the hops on the same path should be scheduled one by one from the first hop to the last hop. We denote the set of directional links of the \( t \)th pairing as \( H^t \), and the set of vertices of the links in \( H^t \) is denoted by \( V^t \). Thus, the problem of optimal scheduling is to find out the directive graph of each pairing to accommodate the traffic of all flows with a minimum of time slots. Our algorithm starts scheduling from the paths with the largest number of hops, and to maximize spatial reuse gain, the algorithm schedules as many links into each pairing as possible with the condition of concurrent transmission satisfied. Since the inherent order of hops in the same path, at most one hop can be scheduled in the same pairing, and the algorithm needs to schedule the preceding hops first.

For each flow \( v \), the set of its transmission paths is denoted as \( P_s(v) \), which can be obtained by the path selection algorithm. For flows not in \( F_{mph} \), its \( P_s(v) \) only has the direct path. From the traffic distribution algorithm, we obtains the traffic demand of each path in \( P_s(v) \). In the transmission scheduling, we denote the number of nodes as \( n \), and the set of selected paths of all flows as \( P_s \), which includes the paths in \( P_s(v) \) for each flow \( v \). For each path \( p \in P_s \), we denote its number of hops as \( h(p) \). For each hop of each path, according to the traffic distributed on this path, we define the number of time slots to accommodate its traffic as the weight of this hop. For the \( i \)th hop link of path \( p \in P_s \), its weight is denoted as \( w_{pi} \). We also denote the \( i \)th hop link of path \( p \in P_s \) as \( (p, i) \). We denote the sender of link (\( p, i \)) by \( s_{pi} \), and the receiver by \( r_{pi} \). The set of hops in \( P_s \) is denoted by \( H \). The hop number of the first hop that is not scheduled on path \( p \) is denoted as \( F_u(p) \). In the \( t \)th pairing, the set of paths that are not visited yet is denoted by \( P_s^t \).

The pseudo-code of the transmission scheduling algorithm is presented in Algorithm 2. First, we obtain the set of paths after path selection. From \( P_s \), we can obtain the set of hops in \( P_s, H \). Since we should start scheduling from the first hop of each path, \( F_u(p) \) for each path \( p \) is set to 1. Then we iteratively schedule each hop of \( H \) into each pairing until all the hops in \( H \) are scheduled, as indicated in line 1. In each pairing, we first find out the unvisited paths with the maximum number of unscheduled hops as in line 6. Then among these paths, the first unscheduled hop with the minimum distance between its weight and current duration of this pairing is selected as the candidate hop of this pairing, as indicated in line 7. This step makes the numbers of time slots of hops in this pairing as close as possible, which can improve the utilization of time slots in this pairing as much as possible. Then the algorithm checks whether this candidate hop is adjacent to the hops already in this pairing since adjacent links cannot be scheduled concurrently, as indicated by line 8. If it is not, first the candidate hop will be added to this pairing, and then the concurrent transmission conditions of this pairing will be checked, as indicated by lines 9–16. If the conditions cannot be met, this candidate hop will be removed from this pairing, as indicated by lines 19–20. Otherwise, the duration of this pairing will updated to accommodate the traffic of this hop as in line 17. Since at most one hop of one path can be scheduled in one pairing, the path where this hop is will be removed from the set of the unvisited paths as in line 22. When the number of links in each pairing reaches \( \lfloor n/2 \rfloor \) or there is no path in the unvisited path set, the algorithm will start scheduling for the next pairing as in line 5, and the scheduling for this pairing will be outputted as in line 24.

Applying this algorithm to the example in section III-B, we obtain the schedule as follows: in the first pairing, link \( A \to D \) of path 3 transmits for one time slot; in the second pairing, link \( A \to C \) of path 2 and \( D \to F \) of path 3 transmit for three time slots; in the third pairing, link \( A \to B \) of path 1 and \( C \to E \) of path 2 transmit for three time slots; in the fourth pairing, link \( F \to B \) of path 3 transmits for one time slot; in the fifth pairing, link \( E \to B \) transmits for two time slots. Thus, it needs 10 time slots to clear the traffic of \( A \to B \). As discussed before, the optimal solution needs 9 time slots. Thus our heuristic scheme obtains nearly the same scheduling solution.

D. Computational Complexity and Control Overhead

The path selection algorithm has the computational complexity of \( \mathcal{O}(n^{H_{max}}) \), where \( n \) is the number of nodes in the network. For the traffic distribution algorithm, its computational complexity is negligible. For the transmission scheduling algorithm, it has the complexity of \( \mathcal{O}(|P_s|n^2) \), where \( P_s \) is the set of selected paths. Thus, the overall complexity of our scheme is \( \mathcal{O}(n^{H_{max}} + |P_s|n^2) \), which is a pseudo-polynomial time solution and suitable for the implementation in practical mmWave WPANs.

With multi-path multi-hop transmissions, there will be increased control overhead since more scheduling information needs to be pushed to the nodes in the WPAN. However, the increase of the control overhead is small with respect to the Gbps transmission rates of mmWave links, and the influence on the performance is minimal.

VI. PERFORMANCE EVALUATION

In this section, we evaluate the performance of our proposed MPMH under various traffic patterns, and compare its performance with the optimal solution scheme and other existing protocols.
Algorithm 2 The Transmission Scheduling Algorithm

Initialization:
1. Input: the set of selected paths of all flows, \( P_s \);
2. Obtain the set of hops in \( P_s \), denoted by \( H \);
3. Obtain the number of hops for each path \( p \in P_s \), \( h(p) \);
4. Obtain the weight of each hop \( (p, i) \in H \), \( w_{pi} \);
5. Set \( F_u(p) = 1 \) for each \( p \in P_s \); \( t=0 \);

Iteration:
1. While \( (|H| > 0) \) do
2. \( t=t+1 \);
3. Set \( V^t = \emptyset \), \( H^t = \emptyset \), and \( \delta^t = 0 \);
4. Set \( P^t_u \) with \( P^t_u = P_s \);
5. While \( (|P^t_u| > 0 \text{ and } |H^t| < n/2) \) do
6. Get the set of unvisited paths with the largest number of unscheduled hops, \( P_{mh} \);
7. Get the hop \( (p, F_u(p)) \) of path \( p \in P_{mh} \) with the minimum \( \text{abs}(\delta^t - w_{pF_u(p)}) \);
8. If \( (s_{pF_u(p)} \notin V^t \text{ and } r_{pF_u(p)} \notin V^t) \) then
9. \( H^t = H^t \cup \{p, F_u(p)\} \);
10. \( V^t = V^t \cup \{s_{pF_u(p)}, r_{pF_u(p)}\} \);
11. For each link \( (p, i) \) in \( H^t \) do
12. Calculate the SINR of link \( (p, i) \), \( SINR_{pi} \)
13. If \( (SINR_{pi} < MS(c_{pi})) \) then
14. Go to line 19
15. End if
16. End for
17. \( \delta^t = \max(\delta^t, w_{pF_u(p)}) \), \( H = H - (p, F_u(p)) \);
18. \( F_u(p) = F_u(p) + 1 \); Go to line 21
19. \( H^t = H^t \setminus \{p, F_u(p)\} \);
20. \( V^t = V^t \setminus \{s_{pF_u(p)}, r_{pF_u(p)}\} \);
21. End if
22. \( P^t_u = P^t_u - p \);
23. End while
24. Output \( H^t \) and \( \delta^t \);
25. End while

A. Simulation Setup

In the simulation, we consider a typical mmWave WPAN of 10 nodes. We assume that all the WNs and the PNC are uniformly distributed in a square area with \( 8m \times 8m \). According to the distances between WNs, we set four transmission rates, 2 Gbps, 4 Gbps, 6 Gbps, and 8 Gbps. There are 10 flows in the network. With \( \varepsilon \) of the criterion in Section V-A set to 0.0625, there is only one flow transmitted through multiple paths, and other flows are transmitted through the direct paths. The paths are selected according to the algorithm in Section V-A. We set the size of data packets to 1000 bytes. We adopt the simulation parameters in Table II of [20], which is also summarized in Table I. The duration of one time slot is set to 5 \( \mu \)s. With the transmission rate of 2 Gbps, a packet can be transmitted in one time slot. As in [11], for the simulated network, the PNC can complete the polling of traffic or schedule pushing in one time slot. Generally, it takes only a few time slots for the PNC to complete path selection and schedule computation. To adapt to dynamical network states, the number of time slots of a frame is bounded by 1000. The simulation length is set to \( 5 \times 10^4 \) time slots. We also set the delay threshold to \( 2.5 \times 10^4 \), and will discard packets with delay larger than the threshold. Initially, each flow has a few packets generated randomly. The maximum number of hops for each selected path, \( H_{max} \), is set to 3. In the simulation, we assume nonadjacent links are able to be scheduled for concurrent transmissions.

In the simulation, we set the following two kinds of traffic modes:

1) Poisson Process: packets arrive at each flow following a poisson process with arrival rate \( \lambda \). The traffic load in this mode, denoted by \( T_1 \), is defined as
\[
T_1 = \frac{\lambda \times L \times V}{R},
\]
where \( L \) is the size of data packets, \( V \) is the number of flows, and \( R \) is set to 2 Gbps.

2) Interrupted Poisson Process (IPP): packets arrive at each flow following an interrupted poisson process (IPP). The parameters of the interrupted poisson process are \( \lambda_1, \lambda_2, p_1 \) and \( p_2 \), and the arrival intervals of an IPP obey the second-order hyper-exponential distribution with a mean of
\[
E(X) = \frac{p_1}{\lambda_1} + \frac{p_2}{\lambda_2},
\]
The interrupted Poisson process can be represented by an ON-OFF process. The ON duration and the OFF duration obey the negative exponential distribution of \( r_1 \) and \( r_2 \), respectively. In the ON duration, packets arrive at each node following the Poisson process of arrival rate \( \lambda_{on\_off} \). While no packet arrives in the OFF duration, \( \lambda_{on\_off}, r_1, \) and \( r_2 \) can be inferred from \( \lambda_1, \lambda_2, p_1, \) and \( p_2 \) as follows.
\[
\lambda_{on\_off} = p_1 \lambda_1 + p_2 \lambda_2, \tag{23}
\]
\[
r_1 = \frac{p_1 p_2 (\lambda_1 - \lambda_2)^2}{\lambda_{on\_off}}, \tag{24}
\]
\[
r_2 = \frac{\lambda_1 \lambda_2}{\lambda_{on\_off}}. \tag{25}
\]
Therefore, IPP traffic is typical bursty traffic. We define the traffic load \( T_1 \) in this mode as:
\[
T_1 = \frac{L \times V}{E(X) \times R}. \tag{26}
\]
We evaluate the system by the following four performance metrics:

1) Average Transmission Delay: The average transmission delay of received packets from all flows, which is in units of
time slots. The average transmission delay does not include the time caused by steering antenna.

2) **Network Throughput:** The number of successful transmissions of all flows until the end of simulation. For a packet of one flow, if its delay is less than or equal to the threshold, it will be counted as a successful transmission. With constant simulation length and fixed packet size, total number of successful transmissions is a good indication to show the throughput performance.

3) **Average Flow Delay:** The average transmission delay of the flow transmitted through multiple paths.

4) **Flow Throughput:** The number of successful transmissions achieved by the flow transmitted through multiple paths.

In order to show the advantages of MPMH, we compare MPMH with the following two protocols:

1) **FDMAC:** The frame-based scheduling directional MAC protocol, and the core of FDMAC is the greedy coloring (GC) algorithm, which can compute near-optimal schedules with respect to the total transmission time with low complexity \([11]\). FDMAC is also a frame based protocol, and in GC, the traffic demand of flows is accommodated by iteratively scheduling each flow into each concurrent transmission pairing in non-increasing order according to traffic demand. To the best of our knowledge, FDMAC achieves the best performance among the existing protocols, such as MRDMAC \([20]\) and MDMAC \([21]\), by fully exploiting spatial reuse in mmWave WPANs.

2) **FDMAC–UR:** FDMAC with links’ differences in the transmission rate not considered, and the transmission rates of all links are set to 1 Gbps.

### B. Comparison with the Optimal Solution

We first compare MPMH with the optimal solution of problem (P2) by the branch-and-bound method. Since obtaining the optimal solutions takes extremely long time, we assume there is only one flow with the traffic to transmit, and the traffic of this flow needs to be transmitted through multiple paths. The traffic load is defined as in \([21]\) and \([26]\) with \(V\) equal to 1. In this case, the delay threshold is set to \(3 \times 10^4\).

The average flow delay and the flow throughput of MPMH and the optimal solution are plotted in Fig. 2. From the results, we can observe that the gap between MPMH and optimal solution is negligible under light load. For the average flow delay, the gap at the traffic load of 5 is only 7.9% of the average flow delay of MPMH. For the flow throughput, the gap is only 5.3% of the flow throughput of MPMH. Therefore, we have demonstrated that MPMH achieves near-optimal performance with low complexity.

![Fig. 2. Comparison between MPMH and the optimal solution under Poisson traffic.](image)

The average execution time of schedule computation for MPMH and the optimal solution is plotted in Fig. 3. From the results, we can observe that MPMH has much less execution time than the optimal solution, and thus it has much lower computational complexity.

![Fig. 3. The execution time of MPMH and the optimal solution under Poisson traffic.](image)

### C. Comparison with Existing Protocols

1) **Delay:** We then evaluate the average network delay of the three MAC protocols. In Fig. 4, we plot it for different traffic loads. From the results, we can observe that with the increase of traffic load, the delay of the three protocols increases, and the delay of FDMAC-UR increases rapidly under light load. MPMH and FDMAC have similar delay performance under light load. Under light load, the arrived packets can be transmitted in a short time, and the frame length is short. Thus, the delay in this case is small. Under heavy load, MPMH outperforms FDMAC and FDMAC-UR. With the traffic load from 4 to 7, compared with FDMAC, MPMH decreases the average transmission delay by about 75.74% under Poisson traffic and 86.54% under IPP traffic on average. For FDMAC-UR, since the actual transmission ability of links is not exploited fully, it has much higher delay compared with MPMH and FDMAC. These phenomena can be explained as follows. In FDMAC and FDMAC-UR, flows cannot be transmitted through multiple paths of multiple hops. Thus, flows with low channel quality on their direct paths will occupy a large number of time slots in the schedule, which increases the frame length significantly and also delay of packets. Since the frame length is bounded by 1000 time slots, the packets that cannot be transmitted are re-scheduled in the next frame. Thus, with the increase of the traffic load, the system enters saturation, and the curves become flat and show a concave form.
As regard to the average flow delay, we present the results in Fig. 5. We can observe that the delay curves of MPMH and FDMAC begin to diverge at the traffic load of 3. Compared with FDMAC, MPMH decreases the delay by about 74.31% under Poisson traffic and 74.29% under IPP traffic on average with the traffic load from 4 to 7, respectively.

2) Throughput: The network throughput achieved by the three protocols is plotted in Fig. 6. We can observe that MPMH has the maximum throughput in all cases, and the gap between MPMH and FDMAC is more significant under heavy load. Under light load, the delay is small, and all the arrived packets can be transmitted successfully for MPMH and FDMAC. Thus, the throughput of MPMH and FDMAC increase linearly under light load. FDMAC stops increasing at the traffic load of 4, while MPMH stops increasing at the traffic load of 6 since the network tends to saturation. For FDMAC-UR, its throughput is poor, and tends to be saturated at the traffic load of 2. Compared with FDMAC, MPMH increases the network throughput with the traffic load from 5 to 10 on average by about 54.37% under Poisson traffic and about 50.58% under IPP traffic, respectively. When traffic load is 10, MPMH outperforms FDMAC by about 80.2%. The reason for MPMH to outperform FDMAC is that in FDMAC, flows with low channel quality on their direct paths cannot be transmitted through multiple multi-hop paths as in MPMH, and occupy a large number of time slots in the schedule, which are underutilized for concurrent transmissions. Under light traffic load, the throughput of MPMH and FDMAC is determined by the traffic arriving at each node. Under heavy traffic load, however, the advantages of MPMH over FDMAC will stand out, and MPMH will outperform FDMAC significantly. On the other hand, with the increase of traffic load, delays of packets increase, and a considerable number of packets are discarded due to their delays exceeding the threshold, which leads to a decrease in FDMAC throughput from the traffic load of 7 and the bigger gap between MPMH and FDMAC at the traffic load of 10.

On the other hand, the flow throughput of the three protocols is presented in Fig. 7. We can observe that the tendencies of the curves are similar to those in Fig. 6. With the traffic load from 5 to 10, MPMH outperforms FDMAC by about 52.14% under Poisson traffic and 47.66% under IPP traffic on average, respectively. The result show that MPMH greatly increases the throughput of the flow of low channel quality compared to FDMAC, especially under heavy traffic loads.

D. Performance under different $H_{max}$

To investigate the impact of the choice of $H_{max}$ on network performance, we plot the average transmission delay and network throughput of MPMH with $H_{max}$ equal to 2, 3, and 4, respectively, in Fig. 8. The traffic mode is the Poisson traffic. From the results, we can observe that MPMH with $H_{max}$ equal to 3 achieves the best performance in terms of delay and throughput. However, the gap between MPMH with different $H_{max}$ is small. For MPMH with $H_{max}$ equal to 2, the advantage of multi-path multi-hop transmissions is limited by the number of hops on paths. For MPMH with $H_{max}$ equal to 4, more hops will lead to larger delay, and with the delays of more packets exceed the threshold, the network throughput also degrades. Therefore, the maximum number of hops on each path, $H_{max}$, should be optimized to achieve an optimal network performance in practice.

We also plot the flow delay and throughput of MPMH with $H_{max}$ equal to 2, 3, and 4, respectively, in Fig. 9. We can observe that the results are similar to those in Fig. 8 and MPMH with $H_{max}$ equal to 3 has the best performance in terms of flow delay and throughput. With a small $H_{max}$ as 2, the number of paths for each flow is limited, and the concurrent transmissions among paths cannot be exploited fully to improve flow delay and throughput performance. With a large $H_{max}$ as 4, transmissions through paths with more hops lead to larger delay, and there are more packets discarded since
their delays exceed the threshold. In practice, $H_{max}$ should be selected according to the actual network conditions to optimize network performance.

![Graph](image)

Fig. 9. Flow Delay and throughput of MPMH with different $H_{max}$ under Poisson traffic.

VII. CONCLUSION

In this paper, we proposed MPMH for mmWave WPANs in the 60 GHz band, which boosts the potential of spatial reuse by transmitting the traffic of flows with low channel quality on their direct paths or with high traffic demand through multiple multi-hop paths to improve throughput and to reduce latency for both these flows and the network. Extensive simulations demonstrate that MPMH achieves near-optimal performance compared with the optimal solution. Compared with FDMAC, MPMH increases flow and network throughput by about 50% and 52.48% on average, respectively. Performance under different maximum number of hops indicates the maximum number of hops should be selected according to the actual network conditions to optimize network performance.

In the future work, we will investigate the accurate and reasonable modeling of NLOS links and try to incorporate NLOS transmission into our scheme. In MPMH, the choice of $\varepsilon$ controls the number of flows transmitted through multiple paths, and we will further optimize $\varepsilon$ according to the actual network conditions such as the channel transmission rate distribution of links and the traffic demand distribution of flows. Although the fairness among flows is improved by the multi-path multi-hop transmission, we will investigate the mechanisms to improve the fairness of our scheme further. Besides, we will also evaluate the energy consumption and energy efficiency of MPMH.

APPENDIX A

NOTATION IN PROBLEM FORMULATION

In order to facilitate the reader to understand the notations in Problem Formulation, we list the notations in Table II as follows.

APPENDIX B

NOTATION IN MPMH

To facilitate the understanding of MPMH, we also list the notations in Table III as follows.

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TABLE II

NOTATION IN PROBLEM FORMULATION

| Symbol | Description |
|--------|-------------|
| $d_v$  | The traffic demand of flow $v$ |
| $M_v$  | The number of flows of flow $v$ |
| $H_{v, p}$ | The number of hops of the $p^{th}$ path of flow $v$ |
| $s_{vp}$ | The traffic demand distributed to the $p^{th}$ path |
| $c_{v, p, i}$ | The transmission rate of $(v, p, i)$ |
| $I_{v, p, u, q, j}$ | A binary variable to indicate if $(v, p, i)$ and $(u, q, j)$ are adjacent |
| $K$ | Number of pairings in a schedule |
| $\delta_k$ | Number of time slots of the $k^{th}$ pairing |
| $d_k$ | A binary variable to indicate whether link $(v, p, i)$ is scheduled in the $k^{th}$ pairing |
| $s_{vp}$ | Sender of link $(v, p, i)$ |
| $r_{vp}$ | Receiver of link $(v, p, i)$ |
| $f_{u, q, j}$ | A binary variable to indicate whether $s_{u, q, j}$ and $r_{v, p}$ direct their beams towards each other |
| $u_{v, p, r_{vp}}$ | The distance between $u_{v, p}$ and $r_{vp}$ |

TABLE III

NOTATION IN MPMH

| Symbol | Description |
|--------|-------------|
| $H_{max}$ | The maximum number of hops for each selected path |
| $s_v$ | The sender of flow $v$ |
| $r_v$ | The receiver of flow $v$ |
| $P(v)$ | Set of all possible paths from $s_v$ |
| $P_{new}(v)$ | Set of generated new paths from $P(v)$ |
| $P_i(v)$ | Set of all possible paths from $s_v$ to $r_v$ |
| $F_{mpmh}$ | Set of flows transmitted through multiple paths |
| $P_1$ | The first node of path $p$ |
| $P_2$ | The last node of path $p$ |
| $c_{p}(p)$ | The lowest transmission rate on path $p$ |
| $h_{p}(p)$ | The hop on path $p$ with the lowest transmission rate |
| $P_s(v)$ | The set of selected paths |
| $H_1(P_s(v))$ | The set of lowest transmission rate hops of paths in $P_s(v)$ |
| $\delta_i$ | Number of time slots of the $i^{th}$ pairing |
| $H^1$ | Set of directional links in the $i^{th}$ pairing |
| $V^1$ | Set of vertices of the links in $H^1$ |
| $n$ | The number of nodes |
| $P_s$ | Set of selected paths of all flows |
| $h(p)$ | Number of hops on path $p$ |
| $s_{pi}$ | The sender of link $(p, i)$ |
| $r_{pi}$ | The receiver of link $(p, i)$ |
| $w_{pi}$ | The weight of link $(p, i)$ |
| $H_i$ | The set of hops in $P_s$ |
| $F_2(p)$ | The hop number of the first unscheduled hop on path $p$ |
| $P_{new}$ | Set of unscheduled paths |
| $P_{inh}$ | Set of unscheduled paths with the largest number of unscheduled hops |
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Yong Niu received B.E. degree in Beijing Jiaotong University, China in 2011. He is currently working toward his PhD degree at the Department of Electronic Engineering, Tsinghua University, China. His research interests include millimeter wave communications, medium access control, and software-defined networks.

Chuhan Gao is an undergraduate student from Tsinghua University, Beijing, China. He is currently working toward the B.E. degree. His research interests include millimeter-wave wireless communications, wireless networks, and software-defined networks.
Yong Li (M’2009) received his B.S. degree in Electronics and Information Engineering from Huazhong University of Science and Technology, Wuhan, China, in 2007, and his Ph.D. degree in electronic engineering from Tsinghua University, Beijing, China, in 2012. During July to August in 2012 and 2013, he worked as a Visiting Research Associate in Telekom Innovation Laboratories (T-labs) and HK University of Science and Technology, respectively. During December 2013 to March 2014, he visited University of Miami, FL, USA as a Visiting Scientist. He is currently a faculty member of the Electronic Engineering at the Tsinghua University. His research interests are in the areas of networking and communications, including mobile opportunistic networks, device-to-device communication, software-defined networks, network virtualization, future Internet, etc. He received Outstanding Postdoctoral Researcher, Outstanding Ph. D Graduates and Outstanding Doctoral thesis of Tsinghua University, and his research is granted by Young Scientist Fund of Natural Science Foundation of China, Postdoctoral Special Find of China, and industry companies of Hitachi, ZET, etc. He has published more than 100 research papers and has 10 granted and pending Chinese and International patents. His Google Scholar Citation is about 440 with H-index of 11, also with more than 120 total citations without self-citations in Web-of Science. He has served as Technical Program Committee (TPC) Chair for WWW workshop of Simpex 2013, served as the TPC of several international workshops and conferences. He is also a guest-editor for ACM/Springer Mobile Networks & Applications, Special Issue on Software-Defined and Virtualized Future Wireless Networks. Now, he is the Associate Editor of EURASIP journal on wireless communications and networking.

Depeng Jin received the B.S. and Ph.D. degrees from Tsinghua University, Beijing, China, in 1995 and 1999 respectively both in electronics engineering. He is an associate professor at Tsinghua University and vice chair of Department of Electronic Engineering. Dr. Jin was awarded National Scientific and Technological Innovation Prize (Second Class) in 2002. His research fields include telecommunication, high-speed networks, ASIC design and future Internet architecture.

Li Su received the B.S. degree from Nankai University, Tianjin, China, in 1999 and Ph.D. degree from Tsinghua University, Beijing, China in 2007 respectively both in electronics engineering. Now he is a research associate with Department of Electronic Engineering, Tsinghua University. His research interests include telecommunication, future internet architecture and on-chip network.

Dapeng Oliver Wu Dapeng Oliver Wu (S’98–M’04–SM06–F’13) received B.E. in Electrical Engineering from Huazhong University of Science and Technology, Wuhan, China, in 1990, M.E. in Electrical Engineering from Beijing University of Posts and Telecommunications, Beijing, China, in 1997, and Ph.D. in Electrical and Computer Engineering from Carnegie Mellon University, Pittsburgh, PA, in 2003.

He is a professor at the Department of Electrical and Computer Engineering, University of Florida, Gainesville, FL. His research interests are in the areas of networking, communications, signal processing, computer vision, and machine learning. He received University of Florida Research Foundation Professorship Award in 2009, AFSOR Young Investigator Program (YIP) Award in 2009, ONR Young Investigator Program (YIP) Award in 2008, NSF CAREER award in 2007, the IEEE Circuits and Systems for Video Technology (CSVT) Transactions Best Paper Award for Year 2001, and the Best Paper Awards in IEEE GLOBECOM 2011 and International Conference on Quality of Service in Heterogeneous Wired/Wireless Networks (QShine) 2006.

Currently, he serves as an Associate Editor for IEEE Transactions on Circuits and Systems for Video Technology, Journal of Visual Communication and Image Representation, and International Journal of Ad Hoc and Ubiquitous Computing. He is the founder of IEEE Transactions on Network Science and Engineering. He was the founding Editor-in-Chief of Journal of Advances in Multimedia between 2006 and 2008, and an Associate Editor for IEEE Transactions on Wireless Communications and IEEE Transactions on Vehicular Technology between 2004 and 2007. He is also a guest-editor for IEEE Journal on Selected Areas in Communications (JSAC), Special Issue on Cross-layer Optimized Wireless Multimedia Communications. He has served as Technical Program Committee (TPC) Chair for IEEE INFOCOM 2012, and TPC chair for IEEE International Conference on Communications (ICC 2008), Signal Processing for Communications Symposium, and as a member of executive committee and/or technical program committee of over 80 conferences. He has served as Chair for the Award Committee, and Chair of Mobile and wireless multimedia Interest Group (MobIG), Technical Committee on Multimedia Communications, IEEE Communications Society. He was a member of Multimedia Signal Processing Technical Committee, IEEE Signal Processing Society from Jan. 1, 2009 to Dec. 31, 2012. He is an IEEE Fellow.