Observations of the Size Distribution of Frazil Ice in an Ice Shelf Water Plume

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Abstract The size distribution of frazil ice is currently unconstrained in ice shelf cavity modeling. Here we observe the time-dependent behavior of the number and size of frazil ice particles in an Ice Shelf Water plume. A novel acoustic scattering inversion was used to infer frazil ice crystal diameters, assuming a log-normal distribution. Observation sites were on land-fast sea ice approximately 13 and 33 km from the front of the McMurdo Ice Shelf, Antarctica. The water column from the ice-water interface to 30 m below mean sea level was monitored over 3 weeks in November of 2016 and 2017. At 15 m below sea level the mean frazil crystal diameter was ~1 mm. Fractional ice volume, derived from frazil crystal size and number density, correlates with in situ supercooling (up to 50 mK at 15 m below sea level). The data presented here provide valuable input for model initiation and evaluation.

Plain Language Summary For the first time we have observed the number and sizes of tiny, disc-like, crystals that appear beneath the springtime sea ice of McMurdo Sound, Antarctica. They are generated by melting at the base of gigantic floating glaciers that surround the Antarctic continent, and are carried out beneath the sea ice in water that is just below its freezing point. From sonar measurements we have found that at 15 m below sea level, there is about one disc-shaped ice crystal with an average diameter of approximately 1 mm in each 10 cm³ of sea water. Previously, there have been no observed sizes of these ice crystals to guide modeling of the interaction between glaciers and the ocean, and our new results provide valuable input for model initiation and evaluation.

1. Introduction

Suspended frazil ice crystals form in turbulent fresh or salt water that is colder than its salinity- and pressure-dependent freezing temperature, a state referred to as in situ supercooled (e.g., Daly, 1984; Martin, 1981; Schneck et al., 2019; Tsang & Hanley, 1985). In natural water bodies in situ supercooling can be generated in numerous ways (Martin, 1981), but two are of particular importance in the Southern Ocean. The first is the rapid heat loss at the surface of open water, for example, in a coastal polynya or a lead, often driven by high winds (e.g., Ito et al., 2015, 2020; Martin, 1981). Alternatively, supercooling may arise through a process known as the “ice pump” (Lewis & Perkin, 1986). The “ice pump” is driven by an intrusion of salty water that causes ice shelf basal melting/dissolving, thereby releasing fresh water of glacial origin at depth in the water column (MacAyeal, 1984). This mixture of colder, fresher water has relatively low density and is therefore buoyant. It rises up the basal slope of the ice shelf and becomes supercooled through the change in its pressure-dependent freezing point (Foldvik & Kvinge, 1974), and frazil crystal formation is initiated (Jenkins & Bombsch, 1995; Smesrud & Jenkins, 2004). The supercooled water can extend beyond the front of the ice shelf and travel beneath adjacent sea ice as part of an Ice Shelf Water (ISW) plume (Hughes et al., 2014; Robinson et al., 2014). The supercooling decays with distance from the ice shelf front (Lewis & Perkin, 1985), as does the influence of the plume on the sea ice cover (Brett et al., 2020; Dempsey et al., 2010; Hughes et al., 2014; Langhorne et al., 2015).

Individual frazil ice crystals in rivers, lakes, and the ocean usually begin as disc-shaped particles, evolving to more irregular shapes as they grow. Collisions cause the crystals to sinter together into groups of particles, known as frazil flocs (e.g., Martin, 1981). In rivers, mean individual frazil crystal diameters are reported between 0.1 and 6 mm (McFarlane et al., 2017), with typical fractional ice volumes in the range 10⁻³ to 10⁻⁶.
Quantitative observations of the shape and size of individual frazil ice particles in salt water of ocean salinity are sparse, with suspended ice crystal diameters ranging 1–3 mm in laboratory experiments (e.g., Martin, 1981; Schneck et al., 2019) and an upper bound of 10–25 mm in the ocean (Dieckmann et al., 1986; Gough et al., 2012; Penrose et al., 1994). Only Schneck et al. (2019) have made laboratory measurements of frazil size distributions in salt water and shown they again follow a log-normal distribution. The ice crystal diameters are ∼13% smaller than in fresh water, with a mean diameter of 0.45 mm, standard deviation 0.31 mm, while flocs have a mean of 1.47 mm and standard deviation of 1.28 mm (Schneck et al., 2019).

McFarlane et al. (2017, 2019) also summarize the methods of detection of suspended frazil in laboratory and river studies. The most successful methods in rivers are high-resolution photography (McFarlane et al., 2017, 2019), and acoustic backscatter techniques (Ghobrial et al., 2013; Marko & Jasek, 2010; Marko et al., 2015; Richard et al., 2011). For the latter, a scattering model is needed to resolve frazil particle size from received sound, and Ghobrial et al. (2013) have used sphere, prolate spheroid, and disk models. Using multifrequency acoustic scattering and assuming a log-normal distribution of equivalent spheres (Marko & Topham, 2015), Marko et al. (2015) have deduced suspended frazil particle size distribution in rivers. In the ocean, where the imperative is to sample a large volume, acoustic techniques have been preferred. Sonar returns (Dieckmann et al., 1986; Ito et al., 2015, 2020; Penrose et al., 1994) and Acoustic Doppler Current Profiler (ADCP) backscatter strength (Ito et al., 2017, 2020; Leonard et al., 2006) are enhanced by suspended frazil ice. Fractional ice volumes are estimated in range 10⁻⁷ to 10⁻⁶ (Ito et al., 2017; Penrose et al., 1994). Thus, salt water observations of the presence, shape and size of suspended frazil ice particles are very limited but laboratory studies indicate particle sizes comparable to freshwater observations (Schneck et al., 2019).

Inclusion of suspended frazil in ocean modeling is well developed (e.g., Jenkins & Bombosch, 1995; Svensson & Omstedt, 1998). Plume models include a range of frazil crystal size classes (e.g., Holland & Feltham, 2005; Hughes et al., 2014; Rees Jones & Wells, 2018; Smedsrud & Jenkins, 2004). Frazil crystal size distribution is also now included in three-dimensional ocean circulation models (Galton-Fenzi et al., 2012). In agreement with observations, modeling suggests the magnitude of the supercooling and the rate of ice crystal deposition depend strongly on distance from the ice shelf (Hughes et al., 2014). Smedsrud and Jenkins (2004) predict that typically, crystals up to ∼2.0 mm in diameter are kept in suspension, and concentrations reach a maximum fractional ice volume of 4.4 × 10⁻⁴. However, model results depend upon the initial frazil crystal size distribution. To date, no measurements exist with which to initiate or validate the output of these model distributions.

In summary, there are presently no measurements of the size distribution of suspended frazil in natural ocean conditions (Ito et al., 2020; Schneck et al., 2019). In this paper we present acoustic observations acquired in 2016 and 2017 from a four-frequency acoustic sounder deployed through sea ice (see Figure 1a). Oceanographic moorings operated alongside to provide simultaneous ocean conditions. A novel acoustic scattering model developed specifically for frazil ice that considers the crystals to be oblate spheroids (Kungl et al., 2020) is used to quantify the time-dependent frazil ice populations formed by the interaction between ice shelves, the ocean and the adjacent sea ice.

2. Methods

2.1. Area Description

McMurdo Sound is an area of seasonally open water bounded by Ross Island, the Antarctic coastline, and the McMurdo Ice Shelf, which is connected to the much larger Ross Ice Shelf (Figure 1a). In McMurdo Sound, the ocean below the land-fast sea ice is seasonally supercooled by up to 45 mK (e.g., Leonard et al., 2011; Lewis & Perkin, 1985; Robinson et al., 2014). The frazil crystals in the supercooled water are driven by buoyancy to settle beneath the sea ice where they form a porous, friable sub–ice platelet layer (Gough et al., 2012; Leonard et al., 2006). This sub–ice platelet layer has been observed to be up to 8 m thick in western McMurdo Sound (Hughes et al., 2014; Langhorne et al., 2015), suggesting this location has a sustained ISW presence where suspended frazil ice crystals are likely to be observed.
2.2. Instrumentation and Data Processing

The acoustic backscattering data were collected by an Acoustic Zooplankton Fish Profiler (AZFP; manufactured by ASL Environmental Science) utilizing four frequency channels: 125, 200, 455, and 769 kHz. The ASL Matlab Toolbox (Version 1.1) was used to convert raw instrument counts to acoustic volume backscattering strength, $S_v$, related to the backscattering cross section, $\sigma_{bs}$. Scattering strength, $S_v$, is smoothed in 11 min spans and spatially averaged over five depth cells of 0.1 m thickness (Frazer, 2019; Kungl et al., 2020).

Typical depth profiles are shown in Figure 1b. The operation of the AZFP is described in more detail in the supporting information and in Kungl et al. (2020).

Kungl et al. (2020) have determined the theoretical acoustic backscattering cross section at frequency $v$ of an individual oblate spheroid, $\sigma_{bs}(v, D)$, with a crystal diameter to thickness ratio of 30 (Dempsey et al., 2010; McFarlane et al., 2014). Assuming a dilute population of such scatterers with random diameter $D$, the total backscattering cross section $\Sigma^{th}_{bs}(v)$ relative to the intensity of the incident plane wave (referenced to 1m) can be modeled by

$$\Sigma^{th}_{bs}(v) = N \int g(D) \sigma_{bs}(v, D) dD,$$

where $N$ is the number density of scatterers and $g$ is the probability distribution of scatterers’ diameter. Following Marko and Topham (2015) and Marko et al. (2015) and supported by recent observations (McFarlane et al., 2015, 2017, 2019; Schneck et al., 2019) and theoretical considerations (Crow & Shimizu, 1988), we choose a log-normal distribution, $g \sim \Lambda(\mu, \sigma)$. We associate $\Sigma^{th}_{bs}(v)$ with the measured backscattering cross section $\Sigma^{obs}_{bs}(v)$. This fitting leads to an optimization algorithm for the yet unknown parameters, $\{\mu, \sigma, N\}$, which minimizes the sum of residual squares $R = \sum_{i=1}^{4} [\Sigma^{th}(v_i) - |\Sigma^{obs}(v_i)|]^2$. Here
Figure 2. (a) Three categories of backscattering strength, $S_v$, shown for the 200 kHz channel, 5–9 November 2017: low (blue, $S_v < -85$ dB), moderate (orange, $-85$ dB $\leq S_v < -45$ dB), and high (yellow, $-45$ dB $\leq S_v$). The three remaining subplots depict the corresponding log-normal parameter distributions: (b) $\sigma$, (c) $\mu_{10} = \log_{10}(\exp(\mu))$, and (d) $\log_{10}N$.

The optimization is carried out at all depths and for all moments in time. A more detailed description of the data processing, choice of parameters (such as aspect ratio, Dempsey et al., 2010; McFarlane et al., 2014, and speed of sound in ice, Ghobrial et al., 2013; Vogt et al., 2008), and uncertainties in the scattering model is available in the supporting information.

We have also collected complementary oceanographic data by moorings comprising a SeaGuard single-depth current meter, SeaBird Electronics SBE-56 thermistors, and SeaBird Electronics SBE-37 microCATs, which recorded current, temperature, and salinity time series, respectively. All oceanographic data are reported here in TEOS-10 using the Gibbs function for seawater thermodynamics (Feistel, 2008), applying the scripts generated by McDougall (2011), and using the latest version of the toolbox available (www.teos-10.org/software.htm). Tidal height forecast data were produced from WWW Tide and Current Predictor for Ross Island, Antarctica.

3. Results

The observations were made at sites 33 km (November 2016) and 13 km (November 2017) from the ice shelf front (see Figure 1a) with the AZFP deployed looking upward from a nominal depth of 30 m. Data sets coincide with significant portions of a spring/neap tidal cycle and were positioned to be within the expected path of the ISW plume emanating from the McMurdo Ice Shelf cavity (Langhorne et al., 2015). At times, especially during the 2017 deployment, the AZFP drifted upward through the water column due to buoyant forces from ice accumulation on the instrument and mooring rope. In Figures 1c and 1d, this is accounted for by using the on-board pressure sensor to determine the AZFP's vertical position in the water column, and adjusting the range bins appropriately.

The AZFP was therefore hauled out of the water to remove ice deposition, and was redeployed within a day. Thus, there are two (effectively) continuous time series of acoustic backscattering in each year for a total of four uninterrupted deployments of 3–7 days each. The times of all observations are reported in NZST.

The site of the oceanographic mooring was approximately 100 m from the AZFP. Supercooling was calculated relative to the salinity- and pressure-dependent freezing point at 15 mBSL using potential temperature and salinity time series at 75 and 100 m depths, respectively. This is achievable because of the remarkable homogeneity of the upper ocean for at least this depth range (Robinson et al., 2014), verified by oceanographic casts taken near the site sporadically throughout the deployments (Robinson, Grant, et al., 2020).

There are depths and times, such as around midnight on 6 November 2017, when there is negligible acoustic signal (i.e., signals $< -100$ dB shown in blue in Figures 1d) indicating that there are few scatterers in the water column. An optimization of such data attempts to characterize a scattering population, even though one probably does not exist. Therefore, we need to select appropriate $S_v$ thresholds to identify physically realistic frazil populations. To demonstrate this process, optimized parameters for 5–9 November 2017 are combined in Figure 2, where they are further sorted into categories based on $S_v$ at 200 kHz. There are noticeably different behaviors of population estimates depending on $S_v$, which are classified as either low ($S_v < -85$ dB), moderate ($-85$ dB $\leq S_v < -45$ dB), or high ($-45$ dB $\leq S_v$).

In general, the moderate scattering strengths lead to physically plausible population parameter estimates: the median size falls into the 0.1–1 mm range, and number densities are less than $10^6$ m$^{-3}$. In contrast, the parameter estimates of low and high scattering strength values often result in an unrealistically large number, for example, $N > 10^{14}$ m$^{-3}$, of very small particles. From here onward, we focus solely on moderate scattering events which comprise 70.4% and 70.1% of measurements in 2017 and 2016, respectively. Further information on data selection is provided in the supporting information.
Figure 3. Optimized parameters, \{\mu, \sigma, N\}, plotted against days in November 2016 (a, c, and e) and November 2017 (b, d, and f), respectively. The $\mu_{10} = \log_{10}(\exp(\mu))$ and $\sigma$ are standard parameters of the log-normal distribution in base 10, while $\log_{10}(N)$ is the number density of crystals per unit volume. Black means “not insonified”; gray “outside $S_v$ thresholds.”

The three parameters yielded by the optimization process, \{\mu, \sigma, N\}, are shown in Figures 3a–3f. Implausible data are in gray. On the assumption that the scatterers are frazil ice crystals, the fractional ice volume, $F$, is calculated (see supporting information) and shown in Figures 4b and 4e, along with the tidal height (Figures 4a and 4d) and supercooling at 15 mBSL (Figures 4c and 4f). In 2017 current speed/direction (Figure 4g) at 100 mBSL is also shown.

As the 2017 deployment is closer to the ice shelf, we display the filtered population parameters, mean and standard deviation of $D$, and number density, $N$, in Figures 5a–5c. In order to obtain a characteristic estimate of a population of frazil crystals, the medians of filtered parameters are taken at 15 mBSL (white line in Figures 5a–5c) in 2017 and found to be $\mu = -7.8$ and $\sigma = 1.3$. The log-normal distribution associated with these parameters is displayed in Figure 5d.

4. Discussion

It is likely that the filtered population of scatterers are frazil ice crystals because the derived fractional ice volume is correlated with supercooling, as demonstrated in Figure 5e at 15 mBSL. The fractional ice volume rises exponentially from $\sim 2 \times 10^{-6}$ to $\sim 8 \times 10^{-6}$ as supercooling increases from 10 to 45 mK. In addition the
supercooling behaves as expected for an ISW plume that is decaying with distance between sites at 13 km (in 2017) and 33 km (in 2016) from the ice shelf front: it hovered around \( \sim 20 \) mK at the distant site, while on 6 November 2017 it rose to \( \sim 40 \) mK at the site closer to the ice front. There the fractional ice volume is greatest (\( \sim 10^{-5} \) to \( 10^{-4} \)) at times following a tidal current from the direction of the ice shelf in the south east (compare Figures 1a, 4e, and 4g). Consequently, the behavior of all optimized parameters and the derived fractional ice volume (see Figures 1a, 3, and 4) is consistent with the interpretation of a mobile population of suspended frazil crystals of fractional ice volume up to \( 10^{-4} \), being carried in a body of supercooled water underneath the sea ice. The magnitude of the fractional ice volume (Figures 4b and 4e) is consistent with observations in rivers (McFarlane et al., 2019).

River frazil diameters are known to be smaller during supercooling that is well established than during the time when supercooling is first imposed upon the water body (McFarlane et al., 2017, 2019). In the present case, the supercooling of the ISW plume has originated some distance from our sites, beneath the ice shelf, and is therefore well established. In addition, smaller crystal diameters are expected in salty ocean waters than in rivers (Schneck et al., 2019). Hence, the small value of the most frequently observed diameter of ocean frazil of 0.07 mm (see the mode of Figures 5d and S2) might be expected. However the mean diameter
Figure 5. Filtered population parameters calculated from the moderate scattering events and plotted against days in November 2017: (a) mean frazil diameter, $D$ (mm), (b) standard deviation of $D$ (mm), and (c) number density, $\log_{10}(N)$ ($m^{-3}$). Black not insonified; gray outside $S_v$ thresholds. (d) Log-normal population density function using the mean parameter values at 15 mBSL in 2017 (median ($\mu$) = $-7.8$ and median ($\sigma$) = $1.3$). The blue dashed line indicates the median frazil diameter ($\approx 0.4$ mm), while the red dash-dotted line represents the mean frazil diameter ($\approx 1.0$ mm). Inset depicts the same information over a logarithmic abscissa. (e) Fractional ice volume, $F$, plotted against supercooling at 15 mBSL, with fitted line (in red).

Derived for McMurdo Sound (1 mm in Figure 5d) is larger than in rivers and saline laboratory experiments ($\approx 0.5$ mm in Schneck et al., 2019). This can be explained by the large standard deviation in our observations (2.2 mm) that skews the McMurdo Sound distribution (see Figures 5d and S2). The broader sample distribution probably arises because crystals are more irregularly shaped in salt water than freshwater (Schneck et al., 2019), and because we are unable to distinguish individual crystals from flocs in our ISW plume observations.

In addition to comparison with previous results in rivers and laboratories, we assess the consistency of the derived fractional ice volume against other geophysical parameters. In November 2017 the sub–ice platelet layer was approximately 3.3 m thick, typical for a negative winter ocean heat flux between 30 and 35 W m$^{-2}$ (Langhorne et al., 2015) and locally equivalent to an ice accumulation of 8–10 mm day$^{-1}$. There are two contributions to the formation of this sub–ice platelet layer: (i) the tiny, suspended frazil crystals observed in the water column rise underneath the sea ice and (ii) they grow larger in situ at the ice-water interface,
where the supercooling is greatest (Leonard et al., 2011; Mahoney et al., 2011; Robinson et al., 2014). We are unable to estimate the latter contribution, so we expect the accumulation of all suspended frazil to be less than 8–10 mm day$^{-1}$, when the daily temporal variation in fractional ice volume (up to $\sim 10^{-3}$) is taken into account. For frazil crystals with diameters up to $\sim 1$ mm, McFarlane et al. (2014) have observed rise velocities up to 9 mm s$^{-1}$, resulting in an accumulation (without in situ growth) of 1–9 mm day$^{-1}$. This is of the same order, but less than, the value derived from the ocean heat flux. Hence, the suspended frazil population parameters are consistent with other geophysical data.

Since we have a crystal size distribution, we can quantify the likelihood of small or large particles, for example, $P(D > 10\text{ mm}) \approx 0.01$, and hence substantiate the occasional observations of large crystals, even with size $\sim 25$ mm (Gough et al., 2012; Penrose et al., 1994). Infrequent large crystals, such as those in the tail of Figure 5d, can have disproportionately large acoustic backscattering and scatter entirely outside the Rayleigh regime due to their size (Kungl et al., 2020; Marko & Topham, 2015).

Considerable frazil accumulation and growth were identified following periods of high scattering activity, both visually upon instrument retrieval and in the rising of the instrument from pressure records (e.g., Figure 1). This suggests an explanation for the horizontal striping that appears toward the end of deployments, and which gradually becomes more pronounced with time (Figures 1–4). We expect that this striping is related to ice attachment to the mooring rope (Leonard et al., 2011; Robinson et al., 2014; Robinson, Grant, et al., 2020) which, with continual growth, gradually enters the insonified volume of water. This assumption is supported by instrument rise after the development of these persistent scatterers in the 2017 deployments (e.g., 13–14 November in Figure 4e), indicating that a large volume of ice was accumulating on the AZFP and rope. However, in 2016 the instrument did not rise considerably due to its greater distance from the ice shelf front.

5. Conclusion

In this paper we provide observational data that constrain the frazil crystal population parameters under sea ice that have previously been unconstrained in models of ice shelf basal processes (Hughes et al., 2014; Smedsrud & Jenkins, 2004). To characterize frazil populations, in situ acoustic and oceanographic data collected in an ISW plume under sea ice in McMurdo Sound for a total of 3 weeks in November 2016 and 2017 have been analyzed within a probabilistic framework based on an oblate spheroidal scattering model (Kungl et al., 2020). The parameters are estimated by an optimization routine comparing the scattering model to the acoustic observations at four frequencies (125, 200, 455, and 769 kHz). At distances between 13 and 33 km from the ice shelf front, and at a depth of 15 m below mean sea level, we have found $\sim 10^6$ to $10^8$ crystals m$^{-3}$ with a mean frazil diameter of approximately 1 mm, hence a fractional ice volume of $\sim 10^{-6}$ to $10^{-5}$. The frazil population parameters respond to the time-dependence of ocean currents and supercooling, with a demonstrated correlation between fractional ice volume and supercooling.

Data Availability Statement

Acoustic and oceanographic data sets for this research are available in the following in-text data citation reference (Robinson, Leonard, et al., 2020).

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