THE FORMATION AND FRAGMENTATION OF PRIMORDIAL MOLECULAR CLOUDS

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ABSTRACT

Many questions in physical cosmology regarding the thermal history of the intergalactic medium, chemical enrichment, reionization, etc., are thought to be intimately related to the nature and evolution of pregalactic structure. In particular, the efficiency of primordial star formation and the primordial initial mass function are of special interest. We present results from high-resolution three-dimensional adaptive mesh refinement simulations that follow the collapse of primordial molecular clouds and their subsequent fragmentation within a cosmologically representative volume. Comoving scales from 128 kpc down to 1 pc are followed accurately. Dark matter dynamics, hydrodynamics, and all relevant chemical and radiative processes (cooling) are followed self-consistently for a cluster-normalized cold dark matter (CDM) structure formation model. Primordial molecular clouds with \( \sim 10^5 \) solar masses are assembled by mergers of multiple objects that have formed hydrogen molecules in the gas phase with a fractional abundance of \( \lesssim 10^{-4} \). As the subclumps merge, cooling lowers the temperature to \( \sim 200 \) K in a "cold pocket" at the center of the halo. Within this cold pocket, a quasi-hydrostatically contracting core with mass \( \sim 200 M_\odot \) and number densities \( \gtrsim 10^5 \text{ cm}^{-3} \) are found. We find that less than 1% of the primordial gas in such small-scale structures cools and collapses to sufficiently high densities to be available for primordial star formation. Furthermore, it is worthwhile to note that this study achieved the highest dynamic range covered by structured adaptive mesh techniques in cosmological hydrodynamics to date.

Subject headings: cosmology: theory — galaxies: formation — methods: numerical

1. INTRODUCTION

Saslaw & Zipoy (1967) realized the importance of gas-phase \( \text{H}_2 \) molecule formation in primordial gas for the formation of protogalactic objects. Employing this mechanism in Jeans-unstable clouds, Peebles & Dicke (1968) formulated their model for the formation of primordial globular clusters. Further pioneering studies in this subject were carried out by Takeda et al. (1969), Matsuda et al. (1969), and Hirasesawa (1969), who followed in detail the gas kinetics in collapsing objects and studied the possible formation of very massive objects (VMOs). In the 1980s the possible cosmological consequences of Population III star formation were assessed (Kashlinsky & Rees 1983; Carr et al. 1984; Couchman & Rees 1986). In particular, Couchman & Rees (1986) discussed first structure formation within the standard cold dark matter (SCDM) model. Their main conclusions were that the first objects might reheat and reionize the universe, raise the Jeans mass, and thereby influence subsequent structure formation.

Early studies focused on the chemical evolution and cooling of primordial clouds by solving a chemical reaction network within highly idealized collapse models (see Hirasesawa 1969; Hutchins 1976; Palla et al. 1983; Mac Low & Shull 1986; Puy & Signore 1996; Tegmark et al. 1997). Some hydrodynamic aspects of the problem were studied in spherical symmetry by Bodenheimer (1986) and Haiman, Thoul, & Loeb (1996). Recently, multidimensional studies of first structure formation have become computationally feasible (Abel 1995; Anninos & Norman 1996; Zhang et al. 1997; Gnedin & Ostriker 1997; Abel et al. 1998a, 1998b; Bromm et al. 1999). These investigations have provided new insights into the inherently multidimensional, nonlinear, nonequilibrium physics that determines the collapse and fragmentation of gravitationally and thermally unstable primordial gas clouds.

In Abel et al. (1998a, hereafter AANZ), we presented the first self-consistent three-dimensional cosmological hydrodynamical simulations of first structure formation in an SCDM-dominated universe. These simulations included a careful treatment of the formation and destruction of \( \text{H}_2 \)—the dominant coolant in low-mass halos (\( M_{\text{tot}} = 10^3–10^8 M_\odot \)), which collapse at high redshifts (\( z \sim 30–50 \)). Among the principal findings of that study were that (1) appreciable cooling only occurs in the cores of the high-density spherical knots located at the intersection of filaments; (2) good agreement was found with semianalytic predictions (Abel 1995; Tegmark et al. 1997) of the minimum halo mass able to cool and collapse to higher densities; and (3) only a small fraction (< 10%) of the bound baryons are able to cool promptly, implying that primordial Population III star clusters may have very low mass. Because of the limited spatial resolution of those simulations (~ 1 kpc comoving), we were unable to study the collapse to stellar densities and address the nature of the first objects formed.

In this paper we present new, higher resolution results using the powerful numerical technique of adaptive mesh refinement (AMR; Bryan & Norman 1997; Norman & Bryan 1998), which has shed some light on how the cooling gas fragments. With an effective dynamic range of 262,144, the numerical simulations presented here are the highest...
resolution simulations in cosmological hydrodynamics to date. Although we are not yet able to form individual protostars, we are able to resolve the collapsing protostellar cloud cores that must inevitably form them. We find that the cores have typical masses ~200 \( M_\odot \), have sizes ~0.3 pc, and have number densities \( n \geq 10^3 \text{ cm}^{-3} \)—similar to dense molecular cloud cores in the Milky Way, with one vital difference: the molecular hydrogen fraction is ~5 × 10^{-4}, meaning that the cores evolve very differently from Galactic cores.

The plan of this paper is as follows. The simulations are briefly described in § 2. Results are presented in § 3. The properties and fate of the primordial protostellar cloud are discussed in § 4. Conclusions follow in § 5. Results of a broader survey of simulations will be reported in Abel, Bryan, & Norman (2000).

2. SIMULATIONS

The three-dimensional AMR calculations presented here use for the hydrodynamic portion an algorithm very similar to the one described by Berger & Colella (1989). The code utilizes an adaptive hierarchy of grid patches at various levels of resolution. Each rectangular grid patch covers some region of space in its parent grid needing higher resolution and may itself become the parent grid to an even higher resolution child grid. Our general implementation of AMR places no restriction on the number of grids at a given level of refinement or on the number of levels of refinement. However, we do restrict the refinement factor—the ratio of parent-to-child mesh spacing—to be an integer (chosen to be 2 in this work). The dark matter is followed with methods similar to the ones presented by Couchman (1991). Furthermore, the algorithm of Anninos et al. (1997) is used to solve the time-dependent chemistry and cooling equations for primordial gas given in Abel et al. (1997). More detailed descriptions of the code are given in Bryan & Norman (1997, 1999) and Norman & Bryan (1998).

The simulations are initialized at redshift 100 with density perturbations of an SCDM model with \( \Omega_m = 0.06 \), \( h = 0.5 \), and \( \sigma_8 = 0.7 \). The abundances of the nine chemical species (\( H, H^+, H^- \), He, He^{+}, He^{++}, H_2, H_2^+, e^- \)) and the temperature are initialized as discussed in Anninos & Norman (1996). After a collapsing high-\( \sigma \) peak has been identified in a low-resolution run, the simulation is reinitialized with multiple refinement levels covering the Lagrangian volume of the collapsing structure. The mass resolution in the initial conditions within this region are 0.53 (8.96) \( M_\odot \) in the gas (dark matter). The refinement criteria ensure that (1) the local Jeans length is resolved by at least four grid zones and (2) no cell contains more than 4 times the initial mass element (0.53 \( M_\odot \)). We limit the refinement to 12 levels within a \( 64^3 \) top grid, which translates to a maximum dynamic range of \( 64 \times 2^{12} = 262,144 \).

3. RESULTS

We find that primordial molecular clouds are only formed at the intersection of filaments, in agreement with the results of AANZ. The evolution of these primordial molecular clouds is marked by frequent mergers yielding highly complex velocity and density fields within the "virial" radius. In the following three sections, we first describe the evolution of these objects and then their morphology and structure.

3.1. Formation of the First Objects

To illustrate the physical mechanisms at work during the formation of the first cosmological object in our simulation, we show the evolution of various quantities in Figure 1. The top panel of this plot shows the virial mass of the largest object in the simulation volume. We divide the evolution into four intervals. In the first, before a redshift of about 35, the Jeans mass in the baryonic component is larger than the mass of any nonlinear perturbation. Therefore, the only collapsed objects are dark-matter-dominated, and the baryonic field is quite smooth. (We remind the reader that a change in the adopted cosmological model would modify the timing, but not the nature, of the collapse.) In the second epoch, \( 23 < z < 35 \), as the nonlinear mass increases, the first baryonic objects collapse. However, these cannot efficiently cool, and the primordial entropy of the gas prevents dense cores from forming. This is shown in the second frame of Figure 1 by a large gap between the central baryonic and dark matter densities (note that while the dark matter density is limited by resolution, the baryonic is not, so the true difference is even larger). As mergers continue and the mass of the largest clump increases, its temperature also grows, as shown in the third panel of this figure. The \( H_2 \) fraction also increases (bottom panel).

By \( z \sim 23 \), enough \( H_2 \) has formed (a few times \( 10^{-4} \)), and the temperature has grown sufficiently high that cooling begins to be important. During this third phase, the central
temperature decreases and the gas density increases. However, the collapse is somewhat protracted because around this point in the evolution the central density reaches $n \sim 10^4$ cm$^{-2}$ and the excited states of H$_2$ are in LTE. This results in a cooling time that is nearly independent of density rather than in the low-density limit where $t_{\text{cool}} \sim \rho^{-1}$ (e.g., Lepp & Shull 1983).

Finally, at $z \sim 19$, a very small dense core forms and reaches the highest resolution that we allowed the code to produce. It is important to note that at this point, the maximum gas density in the simulations exceeds $10^8$ cm$^{-3}$, and at these densities, three-body formation of molecular hydrogen will become dominant (see Palla et al. 1983). Also, the assumption of optical thin cooling begins to break
The increase in dynamic range by $\sim$1000 in the simulations presented here as compared to AANZ allows us to investigate the fragmentation process in detail. Visualizations of the gas density and temperature on two different scales at $z = 19.1$ are shown in Figure 2. In the upper left panel the velocity field is shown superimposed on the density. The $5 \times 10^3 M_\odot$ structure forms at the intersection of two filaments with overdensities of $\sim 10$. Most of the mass accretion occurs along these filaments. The complexity of the velocity field is evident; the accretion shock is highly aspherical and of varying strength. Within the virial radius ($r = 106$ pc), there are a number of other cooling regions. The right-hand panels zoom in on the collapsing fragment. (Note that the smallest resolution element [0.02 pc] in the simulations is still 1600 times smaller than the slice shown in the right-hand panels.) The small fragment in the center of this image has a typical overdensity of $\gtrsim 10^6$ and a mass of $\sim 200 M_\odot$.

3.2. Morphology

The increase in dynamic range by $\sim 1000$ in the simulations presented here as compared to AANZ allows us to investigate the fragmentation process in detail. Visualizations of the gas density and temperature on two different scales at $z = 19.1$ are shown in Figure 2. In the upper left panel the velocity field is shown superimposed on the density. The $5 \times 10^3 M_\odot$ structure forms at the intersection of two filaments with overdensities of $\sim 10$. Most of the mass accretion occurs along these filaments. The complexity of the velocity field is evident; the accretion shock is highly aspherical and of varying strength. Within the virial radius ($r = 106$ pc), there are a number of other cooling regions. The right-hand panels zoom in on the collapsing fragment. (Note that the smallest resolution element [0.02 pc] in the simulations is still 1600 times smaller than the slice shown in the right-hand panels.) The small fragment in the center of this image has a typical overdensity of $\gtrsim 10^6$ and a mass of $\sim 200 M_\odot$.

3.3. Profiles

Despite the complex structure of the primordial molecular clouds, much of their structure can be understood from spherical profiles of the physical quantities, particularly for the dense central core, which is nearly spherical. Figure 3 shows mass-weighted, spherical averages of various quantities around the densest cell found in the simulation at redshift 19.1. Panel a plots the baryonic number density, enclosed baryon mass, and local Bonnor-Ebert mass $M_{\text{BE}} \approx 27 M_\odot T_2^{-1.5} \rho_6^{-1/2}$ versus radius. Panel b plots the abundances of $H_2$ and free electrons. Panel c compares three timescales defined locally: the $H_2$ cooling time $t_{\text{cool}}$, the free-fall time $t_f = [3\pi/(32G)]^{1/2}$, and the sound crossing time $t_{\text{cross}} = r/c_s = 7.6 \times 10^4 r_{\text{pc}} T_2^{-1/2}$ yr. In panel d we identify two distinct regions (labeled I and II) as defined by the temperature profile. Region I ranges from outside the virial radius to $r_{\text{vir}} \sim 5$ pc, the radius at which the infalling material has cooled down to $T_{\text{min}} \sim 200$ K—near the minimum temperature allowed by $H_2$ cooling. Within region I, the temperature profile reflects, in order of decreasing radius, cosmic infall, shock virialization, adiabatic heating in a settling zone, and an $H_2$ cooling flow. In region II, the temperature slowly rises from $T_{\text{min}}$ to $\sim 400$ K as a result of adiabatic heating.

For most of region I the $H_2$ cooling time $t_{\text{cool}}$ is comparable to the free-fall time, as is illustrated in panel c of Figure 3. The $H_2$ number fraction rises from $7 \times 10^{-4}$ to $2 \times 10^{-4}$ as the free electron fraction drops from $2 \times 10^{-4}$ to $2 \times 10^{-5}$. At $r_{\text{vir}}$, the sound crossing time becomes substantially shorter than the cooling time. This suggests that region II is contracting quasi-hydrostatically on the cooling timescale, which approaches its constant high-density value at small radii. This constant cooling time of $\sim 10^5$ yr sets the timescale of the evolution of the fragment until it can turn fully molecular via three-body associations. Inside $r \sim 0.3$ pc, the enclosed baryonic mass of $\sim 200 M_\odot$ exceeds the local Bonnor-Ebert mass, implying that this material is gravitationally unstable. However, as a result of the inefficient cooling, its collapse is subsonic (panel e). The radius where $M > M_{\text{BE}}$ defines our protostellar cloud core.

4. DISCUSSION

Many interesting features of the collapsing and fragmenting “primordial molecular cloud” are identified. Most notable is the formation of an initially quasi-hydrostatically contracting core of $\sim 200 M_\odot$ that becomes gravitationally

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6 Bonnor-Ebert mass is the analog of the Jeans mass but assuming an isothermal ($\rho \propto r^{-2}$) instead of a uniform density distribution.
clusters, then about 6 photons per solar mass is the same as in present-day star formation with 100% efficiency. If the ratio of produced UV photons to the number of UV photons would be liberated by a core the number densities increase from $10^5$ to $10^8$ cm$^{-3}$. For densities $\gtrsim 10^8$ cm$^{-3}$, however, three-body formation of H$_2$ will become the dominant formation mechanism, transforming all hydrogen into its molecular form (Palla et al. 1983). Our chemical reaction network does not include this reaction, and the solution cannot be correct at $r \lesssim 0.1$ pc. The most interesting effect of the three-body reaction is that it will increase the cooling rate by a factor of $\sim 10^3$, leading to a further dramatic density enhancement within the core. This will decrease the dynamical timescales to $\lesssim 100$ yr, effectively decoupling the evolution of the fragment from the evolution of its host primordial molecular cloud. Therefore, it is a firm conclusion that only the gas within these cores can participate in Population III star formation.

Omukai & Nishi (1998) have simulated the evolution of a collapsing, spherically symmetric primordial cloud-to-stellar density including all relevant physical processes. Coincidentally, their initial conditions are very close to our final state. Based on their results, we can say that if the cloud does not break up, a massive star will be formed. Adding a small amount of angular momentum to the core does not change this conclusion (Bate 1998). A third possibility is that the cloud breaks up into low-mass stars via thermal instability in the quasi-hydrostatic phase. Silk (1983) has argued that, as a result of the enhanced cooling from the three-body–produced H$_2$, fragmentation of this core might continue until individual fragments are opacity limited (i.e., they become opaque to their cooling radiation). Exploring which of these scenarios is correct will have to await yet higher resolution simulations including the effects of radiative transfer. It will also be interesting to examine the possible effects of molecular HD, which, although much less abundant, is a much more efficient coolant at low temperatures.

How many cores are formed in our halo? Because our time step contracts rapidly once the first core forms, we are not yet able to answer this question definitively. An earlier, less well resolved simulation yielded 5–6 cores by $z = 16.5$, suggesting that multiple cores do form. We speculate that the total number of cores to eventually form will be proportional to the total amount of cooled gas. However, the first star in a given halo will most likely always be formed close to its center, where the dynamical timescale is shortest. The cooling timescale at $r_{T_{\text{min}}}$ (in Fig. 3) of $\gtrsim 10^8$ yr should roughly correspond to the typical formation time of fragments. During this time the product of the first collapsed fragment might already be an important source of feedback. Hence, even for the question of the efficiency of fragmentation it seems that feedback physics has to be included.

Let us assume that the first $\sim 200 M_\odot$ cores fragment to form stars with 100% efficiency. If the ratio of produced UV photons per solar mass is the same as in present-day star clusters, then about $6 \times 10^{63}$ UV photons would be liberated during the average lifetime of a massive star ($\sim 5 \times 10^7$ yr). This is about 100 times more than the $\sim 4 \times 10^{61}$ hydrogen atoms within the virial radius. However, the average recombination time $(nk_{\text{rec}})^{-1} \sim 5 \times 10^5$ yr within the virial radius is a factor of 100 less than the average lifetime of a massive star. Hence, very small or zero UV escape fractions for these objects are plausible. However, the first supernovae and winds from massive stars will substantially change the subsequent hydrodynamic and chemical evolution as well as the star formation history of these objects. A more detailed understanding of the role of such local feedback will have to await yet more detailed simulations that include the poorly understood physics of stellar feedback mechanisms.

Since the collapsing core evolves on much faster timescales than the rest of the halo, it seems plausible that the first star (or star cluster) will have a mass less than or of the order of the core mass. It seems also quite clear that the radiative feedback from this star (these stars) will eventually halt further accretion. As a consequence, this might suggest that the formation of very massive objects or supermassive black holes is unlikely. The latter speculation will be tested by yet higher resolution simulations, which we are currently working on.

Recently, Bromm, Coppi, & Larson (1999) have studied the fragmentation of the first objects in the universe. The results of their simulations using a smooth particle hydrodynamics technique with isolated boundary conditions disagree with the results presented here. Their objects collapse to a disk that then fragments quickly to form many fragments throughout the rotationally supported disk. The efficiently fragmenting disk in those simulations originates from the assumed idealized initial conditions. These authors simulated top-hat spheres that initially rotate as solid bodies on which smaller density fluctuations were imposed. Naturally, they find a disk. It is also clear from their top-hat assumption that if the disk breaks up, it will do so everywhere almost simultaneously. Our results with realistic initial conditions show clearly that a rotating top hat is a gross oversimplification.

5. CONCLUSIONS

We have reported first results from an ongoing project that studies the physics of fragmentation and primordial star formation in a cosmological context. The results clearly illustrate the advantages and power of structured AMR cosmological hydrodynamic methods to cover a wide range of mass, length, and timescales. All findings of AANZ are confirmed in this study. Among other things, these are that (1) a significant number fraction of hydrogen molecules is only formed in virialized halos at the intersection of filaments and (2) only a small percentage of the halo gas has cooled to $T < T_{\text{vir}}$.

The improvement of a factor of $\sim 1000$ in resolution over AANZ has given new insights into the details of the fragmentation process and constraints on the possible nature of the first structures: (1) only $\lesssim 1%$ of the baryons within a virialized object can participate in Population III star formation; (2) the formation of supermassive black holes or very massive objects in small halos seems very unlikely; (3) fragmentation via Bonnor-Ebert instability yields a $\sim 200 M_\odot$ core within one virialized object; (4) if the gas were able to fragment further through three-body H$_2$ association and/or opacity limited fragmentation, only a small fraction of all baryons in the universe would be converted into small mass objects; (5) the escape fraction of UV photons above the Lyman limit should initially be small as a result of the high column densities of H I ($N_{\text{HI}} \sim 10^{23}$ cm$^{-2}$) of the parent primordial molecular cloud; and (6) the first star in
the universe is most likely born close to the center of its parent halo of $\gtrsim 10^5 M_\odot$.

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