First elastic electron scattering from $^{132}$Xe at the SCRIT facility

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The first elastic electron scattering has been successfully performed at the self-confining RI ion target (SCRIT) facility, the world’s first electron scattering facility for exotic nuclei. The SCRIT technique achieved high luminosity (over $10^{27} \text{cm}^{-2}\text{s}^{-1}$, sufficient for determining the nuclear shape) with only $10^{8}$ target ions. While $^{132}$Xe used in this time as a target is stable isotope, the charge density distribution was firstly extracted from the momentum transfer distributions of the scattered electrons by comparing the results with those calculated by a phase shift calculation.

The charge density distribution of the nucleus is one of the most important factors in the nuclear structure investigations, as it directly relates to the superimposition of the squared wave functions of all protons in the nucleus. Following the monumental measurements by R. Hofstadter and his colleagues [1] in the latter half of the 20th century, many stable nuclei have been studied by elastic electron scattering experiments. However, with few exceptions, electron scattering from short-lived unstable nuclei has been precluded by the difficulty in preparing the target material for these nuclei. Realizing electron scattering for unstable nuclei has been long awaited, as it has been revealed that some of nuclei far from the stability valley exhibit exotic features such as neutron halo, neutron skin, etc. [2] which are totally unknown in stable nuclei.

We have invented an internal target-forming technique called self-confining RI ion target (SCRIT) [3] in an electron storage ring, which three-dimensionally traps the target ions along the electron beam axis. The ions are confined by transverse focusing force given by the electron beam itself and an electrostatic potential well provided by electrodes put along the beam axis. After a successful feasibility study [4, 5], we have recently completed the construction of the SCRIT electron scattering facility [6] at RIKEN’s RI Beam Factory, which is dedicated to the study of exotic nuclei. The luminosity required for elastic electron scattering ($10^{27} \text{cm}^{-2}\text{s}^{-1}$) was achieved with only $10^{8}$ target ions as available at an conventional isotope separation on line (ISOL) facility. In traditional electron scattering experiments, the number of target nuclei is typically of the order of $10^{20}$. This advancement enables electron scattering not only from unstable nuclei, but also from stable nuclei that have not been studied to date.

In this Letter, we report the first elastic electron scattering results of $^{132}$Xe nuclei obtained at the SCRIT facility. Although $^{132}$Xe is a stable nucleus, it has never been investigated by electron scattering [7]. Interestingly, stable xenon isotopes have been recently utilized as targets for dark matter searches [8] [10], and in neutrinoless double beta decay experiments [11]. To calculate the cross sections in these experiments, the form factors of the Xe isotopes are required. However, transition X-ray measurements of muonic atoms have yielded only the root-mean-squares of the Xe isotopic charge radii [12]. In the present study, we newly determine the surface shape of the $^{132}$Xe nucleus in the Xe isotopes.

Figure 1 illustrates the SCRIT facility. Details of the facility are described elsewhere [6, 13]. The 150 MeV electron beam is injected and accumulated in the storage ring (SR2). The electron beam is then accelerated to the desired energy below 700 MeV if necessary. The Xe ions are produced from natural Xe gas, and accelerated and mass-separated by functions of an electron-beam driven RI separator for SCRIT (ERIS) [14]. Continuous ion beam from the ERIS is converted to pulsed beam with the duration of 370 µs at a fringing-RF-field-activated ion beam compressor (FRAC) [15] and it is delivered to the SCRIT. The scattered electrons from confined ions in the SCRIT are then detected by a window-frame spectrometer for electron scattering (WiSES). The luminosity is experimentally determined by counting the bremsstrahlung photons (produced by collisions with target ions) with a luminosity monitor (LMon) put at 8-m downstream from the SCRIT.

The SCRIT device is composed of four cylindrical electrodes surrounding the electron beam. The middle two electrodes define the trapping length of 50 cm in total, and they are separated with 1-cm gap to provide a space for insertion of a tungsten wire, which was used for the study of the spectrometer acceptance. These electrodes form an electrostatic potential lower than the acceleration voltage of delivered target ions by a few V to make the ion motion slow and to make confinement time longer. Electrodes at both ends make barrier potentials for the longitudinal confinement.

The $^{132}$Xe ions were trapped in the SCRIT for 240 ms, then ejected to refresh the target quality, although the confinement lifetime for target ions is typically 2–3 s.
The ejection was implemented by controlling one of the gate potentials on the SCRIT device. Ejection reduces the contribution of residual gas which becomes ionized and trapped by the electron beam, and hence accumulates over time. To estimate the background (contributed mainly by the residual gases), the injection-trapping-ejection sequences was alternately repeated with and without the target ions at 10-ms intervals. The number of $^{132}$Xe ions introduced to the SCRIT with each cycle was less than a few times $10^8$.

The WiSES spectrometer consists of a dipole magnet, drift chambers at the entrance and exit of the magnet, two scintillation counters for trigger generation, and a helium-gas filled bag constructed from a 30 µm-thick vinyl. The bag is installed between the two drift chambers to reduce the multiple-scattering effect. The spectrometer magnet is a window-frame dipole magnet with a large aperture. Its dimensions are 29 cm (H), 171 cm (W), 140 cm (D), and its magnetic field is uniform except at the inlet and outlet. The trajectories of the scattered electrons are reconstructed using a three-dimensional field map calculated by a finite element method (TOSCA [16]). The calculated map was confirmed to well-reproduce the vertical component of the magnetic field measured with a hall probe. During measurements, the magnitude of the magnetic field was monitored by an NMR probe positioned in the homogeneous field region. The width of the vertical distribution was 6.3 mm ($\sigma$), consistent with the vertical position resolution evaluated by using the wire target. The shaded histograms in Fig. 2(a) and (c) are the background contributions from residual gases measured in the absence of target ions. These contributions were approximately estimated as 10%, 30%, and 40% for $E_e$ = 151, 201, and 301 MeV, respectively. Assuming $^{16}$O as the residual gas, the approximate background luminosity was estimated as $1 \times 10^{27}$ cm$^{-2}$s$^{-1}$, roughly consistent with the estimation from vacuum pressure ($\sim$5×$10^{-8}$ Pa around the SCRIT region).

Figure 3 shows the reconstructed momentum spectra at $E_e$ = 151, 201, and 301 MeV, obtained after subtracting the background. Elastic events clearly mani-
The measured $\delta p/p$ were $\sim 5.4 \times 10^{-3}$, $3.7 \times 10^{-3}$, and $3.0 \times 10^{-3}$, respectively. The present momentum resolutions are slightly below the design values. Possible reasons for this discrepancy are the imperfection of knowledge in the magnetic field of the spectrometer, a small amount of air contamination in the helium bag, and the energy spread of the electrons circulating in the SR2. As shown in the figure, the low-energy tails below the elastic peak at $E_e = 151$ MeV and 201 MeV were well-reproduced by simulations of a well-known radiative process. At $E_e = 301$ MeV, the enhanced tail suggests some inelastic processes. In the high-momentum transfer region (0.9–1.4 fm$^{-1}$), the magnitude of elastic scattering diminishes and inelastic scattering processes (such as the giant dipole resonance) gain prominence.

![Figure 2](image2.png)

**FIG. 2.** Reconstructed vertex distributions of the $^{132}$Xe target at $E_e = 151$ MeV. The low-energy background is rejected by the momentum selection. The top and bottom of the SCRIT electrodes are placed at ±20 mm in vertical position. Panels (a) and (c) show the vertex point distributions with and without the target ions (plain and hatched histograms, respectively).

The lines in Fig. 3 are the elastic scattering cross sections calculated by a phase shift calculation code DREPHA with a nuclear charge density distribution. The solid line assumes a two-parameter Fermi distribution $\rho(r) = \rho_0/(1 + \exp(4.4(r-c)/t))$, where $\rho_0$ is the density at the center of the nucleus, and $c$ and $t$ are surface distribution parameters. In the present analysis, the luminosity at each energy was considered as a fitting parameter. Determination of the absolute luminosity by LMon is currently underway. The luminosities evaluated by fitting the two-parameter Fermi distribution were $0.87 \times 10^{27}$, $1.06 \times 10^{27}$, and $1.55 \times 10^{27}$ cm$^{-2}$s$^{-1}$ for $E_e = 151$, 201, and 301 MeV, respectively, in which best values of the parameters $c$ and $t$ are used as evaluated later (see Fig. 4). The dashed line is the calculation with the Hartree-Fock calculation proposed by Lapikás, which phenomenologically incorporates the shell effect by interpolation between the Hartree-Fock calculations of neighboring nuclei, $^{124}$Sn and $^{138}$Ba. The dotted line is calculated by using the beyond-relativistic-mean-field theory in Mei. In the both calculations, only the luminosities were considered as fitting parameters because the nuclear shapes are fixed. In general, the both theoretical calculations agree with our data within the experimental errors. The experimental data are expected to be contaminated with inelastic scattering processes corresponding to some excited states (e.g., $2^+$, excitation energies are 0.67 MeV, 1.3 MeV and higher), because the momentum resolution of our spectrometer is insufficient for separating these states from the ground state. Theoretical calculations with a distorted wave Born approximation code FOBES using a transition density distribution indicate that below 1.2 fm$^{-1}$ and at 1.4 fm$^{-1}$, the first excited state contributes below 1% and 10% of the ground-state contribution, respectively. These contributions are much smaller than the statistical errors.

![Figure 3](image3.png)

**FIG. 3.** Reconstructed momentum spectra of $^{132}$Xe target after background subtraction. Red shaded lines are the simulated radiation tails following the elastic peaks.

Figure 4 shows differential cross sections of the $^{132}$Xe multiplied by luminosity, as functions of effective momentum transfer ($q_{eff}$) for $E_e = 151, 201$ and 301 MeV. The $q_{eff}$, which accounts for the Coulombic attraction between electrons and nuclei, is defined as, $q_{eff} = q (1 + \frac{1}{2} (Z \alpha/E_{i} R))$, $R = 1.2 \times A^{1/3} \text{ fm}$ [13]. In this expression, $q$ is the momentum transfer calculated from the measured angle as $q = 2E_i \sin(\theta/2)$, $E_i$ is the initial electron energy, and $\theta$ is the polar angle of the scattered electrons. $Z$ and $A$ are the atomic and mass numbers of the nucleus respectively, and $\alpha$ is the fine structure constant. The systematic error in the cross section, introduced by ambiguity in the spectrometer acceptance, was estimated as approximately 5%.

The lines in Fig. 4 are the elastic scattering cross sections calculated by a phase shift calculation code DREPHA with a nuclear charge density distribution. The solid line assumes a two-parameter Fermi distribution $\rho(r) = \rho_0/(1 + \exp(4.4(r-c)/t))$, where $\rho_0$ is the density at the center of the nucleus, and $c$ and $t$ are surface distribution parameters. In the present analysis, the luminosity at each energy was considered as a fitting parameter. Determination of the absolute luminosity by LMon is currently underway. The luminosities evaluated by fitting the two-parameter Fermi distribution were $0.87 \times 10^{27}$, $1.06 \times 10^{27}$, and $1.55 \times 10^{27}$ cm$^{-2}$s$^{-1}$ for $E_e = 151$, 201, and 301 MeV, respectively, in which best values of the parameters $c$ and $t$ are used as evaluated later (see Fig. 4). The dashed line is the calculation with the Hartree-Fock calculation proposed by Lapikás, which phenomenologically incorporates the shell effect by interpolation between the Hartree-Fock calculations of neighboring nuclei, $^{124}$Sn and $^{138}$Ba. The dotted line is calculated by using the beyond-relativistic-mean-field theory in Mei. In the both calculations, only the luminosities were considered as fitting parameters because the nuclear shapes are fixed. In general, the both theoretical calculations agree with our data within the experimental errors. The experimental data are expected to be contaminated with inelastic scattering processes corresponding to some excited states (e.g., $2^+$, excitation energies are 0.67 MeV, 1.3 MeV and higher), because the momentum resolution of our spectrometer is insufficient for separating these states from the ground state. Theoretical calculations with a distorted wave Born approximation code FOBES using a transition density distribution indicate that below 1.2 fm$^{-1}$ and at 1.4 fm$^{-1}$, the first excited state contributes below 1% and 10% of the ground-state contribution, respectively. These contributions are much smaller than the statistical errors.
and \( \langle r^2 \rangle^{1/2} = 4.787 \pm 0.1 \text{ fm} \). The large error in the diffuseness in the present analysis is due to the absence of the experimentally determined absolute value of the luminosity. This deficiency will be improved by the LMon development.

Our calculated root-mean-square charge radius is consistent with that obtained by X-ray measurements of muonic atoms, namely, \( \langle r^2 \rangle^{1/2} = 4.787 \text{ fm} \). It is worth noting that the theoretical root-mean-square charge radii reported by Lapikás [20] and Mei [22] (4.804 fm and 4.806 fm respectively) also lie within the error bounds of our result.

In conclusion, we extracted information on the nuclear shape of \(^{132}\text{Xe}\) by measuring the elastic electron scattering from \(^{132}\text{Xe}\) at the SCRIT electron scattering facility. The momentum transfer distributions of the differential cross sections are mostly consistent with theoretical calculations; especially, the root-mean-square charge radii agree within the experimental errors. Assuming the two-parameter Fermi distribution model as the nuclear charge density distributions and electron shape parameters \( c \) and \( t \), the three data sets \((E_e = 151, 201, \text{ and } 301 \text{ MeV})\) are fitted simultaneously. Slanted lines are curves of constant root-mean-square charge radii. The 4.787 fm line represents the result of X-ray measurements of muonic atoms [12].

FIG. 5. Contour \( \chi^2 \) plot of parameter determination, obtained by fitting to DWBA calculations with different nuclear shape parameters \( c \) and \( t \). The three data sets \((E_e = 151, 201, \text{ and } 301 \text{ MeV})\) are fitted simultaneously. Slanted lines are curves of constant root-mean-square charge radii. The 4.787 fm line represents the result of X-ray measurements of muonic atoms [12].

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