A catalogue of temperatures for Kepler eclipsing binary stars

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ABSTRACT

We have combined the Kepler Eclipsing Binary Catalogue with information from the HES, KIS and 2MASS photometric surveys to produce spectral energy distribution fits to over 2600 eclipsing binaries in the catalogue over a wavelength range of 0.36–2.16 Å. We present primary (T1) and secondary (T2) stellar temperatures, plus information on the stellar radii and system distance ratios. The derived temperatures are on average accurate to 370 K in T1 and 620 K in T2. Our results improve on the similarly derived physical parameters of the Kepler Input Catalogue through consideration of both stars of the binary system rather than a single star model, and inclusion of additional U-band photometry. We expect these results to aid future uses of the Kepler eclipsing binary data, both in target selection and to inform users of the extremely high-precision light curves available. We do not include surface gravities or system metallicities, as these were found to have an insignificant effect on the observed photometric bands.

Key words: catalogues – binaries: close – binaries: eclipsing – binaries: general.

1 INTRODUCTION

In preparation for the Kepler mission, Brown et al. (2011) produced the Kepler Input Catalog (KIC), providing spectral energy distribution fit parameters for stars in the Kepler field of view. Since then the Kepler satellite has produced high-precision light curves for some 150 000 stars in this field, many of which have proven to be eclipsing binaries. These are catalogued in the Kepler Eclipsing Binary Catalogue (KEBC; Prsa et al. 2011; Slawson et al. 2011; Matijević et al. 2012), and number well over 2000. With this catalogue as a guide, many interesting results have been found (e.g. Carter et al. 2011; Armstrong et al. 2012; Bloemen et al. 2012; Rappaport et al. 2012; Lee et al. 2013) not least those of the circumbinary planets (e.g. Doyle et al. 2011; Welsh et al. 2012). The parameters presented by the KIC are used in target selection for both the primary Kepler purpose of planet hunting and other guest observer programmes, as well as to provide estimated radii for candidate planets (Batalha et al. 2013). They have been subject to latter testing, through for example population synthesis (Farmer, Kolb & Norton 2013).

Here, we aim to produce a catalogue similar to the KIC for the eclipsing binary (EB) systems of the KEBC, taking into account our new knowledge of their binary nature with the information presented by the various photometric surveys of the Kepler field. In this way, we can improve upon the KIC for these binary systems, through extended wavelength coverage (particularly inclusion of the U band) and consideration of both stars. Although the primary star often dominates the observed flux, not including the secondary (as in the KIC) can lead to biases.

The structure of the paper is as follows. We lay out our input data in Section 2, and explain the model used to fit the observed colour bands in Section 3. We test the model against simulated stellar parameters in Section 3.2, and present our result catalogue and parameter distributions in Section 4, while Section 5 discusses the results and observed distributions.

2 DATA

2.1 Kepler Eclipsing Binary Catalogue

We make use of data from the KEBC. Our targeted objects’ KIC identification numbers (KIC IDs) are taken from the catalogue, along with the primary and secondary eclipse depth ratio, which were used to produce an estimate of the temperature ratio T2/T1 of each binary as described in Section 3.1.3. We took a version of the KEBC as presented online on 2013 September 18 to give KIC IDs and eclipse depth ratios, yielding 2610 systems. 13 of these systems contained multiple entries in the catalogue, we took the first entry only in each of these cases. Specific KIC IDs used are presented with our results in Section 4.

2.2 Howell–Everett Survey (HES)

We use photometry from the HES (Everett, Howell & Kinemuchi 2012). The survey consists of the three optical filters Johnson U, B and V, in the Vega system (Morgan, Harris & Johnson 1953), and...
contains data on 2424 objects of the 2610 from the KEBC. Errors were taken as presented in the KIC catalogue.

2.3 KIS

In parallel to the HES, we use data from the Kepler INT Survey (KIS; Greiss et al. 2012a,b, Data Release 2. This allows models to be fitted to two independent sets of photometry separately, increasing reliability and allowing bad data to be more easily flagged. The KIS provides data in the RGO $U$, Sloan $g$, $r$ and $i$ bands, in the Vega system. Errors provided in the catalogue are photometric only, we add systematic errors to the photometric errors in quadrature. We use table 3 of Greiss et al. (2012a), which gives the systematic offset used in calibrating each band to the KIC, as an estimation of the systematic error for each band (a 0.05 mag systematic error was used for the $U$ band).

Some objects in the KIS are observed more than once, these are available as separate sets of data, duplicates or triplicates (no object had more than three sets of data), for the same object. There are 2439 of the KEBC systems present in the KIS, of which 764 are duplicates and 111 triplicates. These multiple data set systems were treated as independent objects during the subsequent analysis. Data for individual bands were filtered using the KIS class flag. Only bands of data with class $-1$ (stellar) or $-2$ (probably stellar) were used.

2.4 2MASS

To each of the HES and KIS surveys, we added data from 2MASS (Skrutskie et al. 2006). This consisted of the Johnson $J$, $H$ and 2MASS specific $K_s$ bands, in the Vega system. The combined total photometric uncertainties were used as presented in the 2MASS catalogue. Data were accepted if the SNR in that band was $\geq 5$ and the object was not flagged as blended or contaminated. 2590 objects were found in the 2MASS catalogue.

2.5 Combination

For each object, the above survey data were combined to produce two partially independent data sets, HES + 2MASS, hereafter UB-VJHK, and KIS + 2MASS, hereafter UgrJHK. Each data set is treated as independent objects during the subsequent analysis. Data for individual bands were filtered using the KIS class flag. Only bands of data with class $-1$ (stellar) or $-2$ (probably stellar) were used.

3 MODEL

3.1 Setup

We use a Markov Chain Monte Carlo (MCMC) code utilizing the Metropolis–Hastings algorithm, enacted using the Python module PyMC (Patil, Huard & Fonnesbeck 2010). We assumed each system to be composed of two stars, and fitted the combined contribution from these two stars to the observed colour data. This intrinsically assumes that the data were taken when the stars were out of eclipse. This is reasonable for many eclipsing binaries, for those in overcontact systems (where the two stars are permanently in contact), it is less so but hard to avoid. In these cases, it is only the apparent radii of the eclipsed star which will change; this is in general fitted poorly anyway (see Section 3.2), and the fitted temperatures should be unaffected.

3.1.1 Model atmospheres

We use the Castelli–Kurucz 04 (CK04) model atmospheres (Castelli & Kurucz 2004). These cover a grid of $[3500 < T < 50000 \text{K}]$, $[-2.5 < [M/H] < 0.5]$ and $[0.0 < \log g < 5.0]$, of which for computing efficiency purposes we used temperatures up to 13 000 K (some systems were run with higher temperature limits, see Section 4.1). The grid spacing was 250 K in temperature (1000 K for atmospheres above 13 000 K), 0.5 in $[M/H]$ (with an additional point at $[M/H] = 0.2$) and 0.5 in $\log g$. Model values were interpolated linearly between the two closest grid points of each parameter. Although the CK04 atmospheres depend on surface gravity and metallicity as well as temperature, we found that they were retrieved extremely poorly (see Section 3.2). As such we did not include them in our model, using CK04 atmospheres with the KIC surface gravity and zero metallicity for each system.

To make use of the CK04 atmospheres, they must be integrated over a response function for the relevant filter to produce band-integrated flux densities. We used filter transmission curves as detailed in the respective papers of the HES and KIS. For the 2MASS data, relative spectral response functions from Cohen, Wheaton & Megeath (2003) were used. These provide an absolute flux calibration using the calibrated spectrum of Vega, matching with the Vega system magnitudes of the HES and KIS.

3.1.2 Interstellar extinction

We use the extinction relations of Cardelli, Clayton & Mathis (1989) with a constant $R_V$ of 3.1, resulting in two analytical relations relevant for optical wavelengths ($U$–$i$) and IR wavelengths ($JHK$). This allowed extinction in each band to be calculated as a function of that of the $V$ band. The specific conversion factor for each photometric band depends on the spectrum of the star under question (due to the distribution of stellar flux within the band), but we found that making the simplifying assumption of an extinction factor for each band calculated at the central wavelength of the relevant band had negligible effect for the stars considered here. We took $V$-band extinctions from the $A_V$ values of the KIC, and used the mean value of the KIC EBs of 0.4 mag for systems where no KIC values were available. This is applied to 244 systems of the 2610; these systems are flagged in the presented catalogue. While the KIC values for $A_V$ are by no means perfect (see Brown et al. 2011 for a full discussion), we found that fitting them ourselves did not constrain them, and results in an additional free parameter in what is already a large parameter space. As such we use the KIC values both to constrain the parameter space and to allow easier comparison between our results and the $T_{eff}$ of the KIC.

3.1.3 Generation of $T_2/T_1$

As direct values for $T_2/T_1$ were not available at the time of submission, we estimate them from the ratio of secondary to primary eclipse depth (as $T_2/T_1 \approx (\text{depth}_{\text{sec}}/\text{depth}_{\text{pri}})^{0.25}$. For circular binaries, this represents a good proxy for the temperature ratio. For increasingly eccentric orbits, due to the possibility of different surface areas being occulted in primary and secondary eclipse, the eclipse depth ratio becomes an increasingly less accurate estimator of $T_2/T_1$. We formed a distribution for $T_2/T_1$ by including (1) the known parameters (period, eccentricity, argument of periapse) of each binary, (2) measurement scatter in recovering the eclipse depths (Gaussian errors of 0.025 and 0.05 for over contact and non-overcontact binaries, respectively, from the test figs 8 and 10 of Prsa...
et al. 2011) and (3) a correction for the effect of eccentricity, derived for each binary individually. For full details see Appendix A.

3.1.4 Fit parameters

Four fit parameters were used. These comprised the primary star temperature $T_1$, secondary star temperature $T_2$ (constrained through the temperature ratio as measured from the light curves), radius ratio of the stars $R_2/R_1$ and the primary radius to system distance ratio $R_1/D$. Note that stellar radii as used provide no allowance for non-sphericity of stars, and as such represent an ‘effective radius’, particularly in the case of overcontact EB systems. No constraining relations were used, each parameter was allowed to vary according to its prior (see Section 3.1.5). Observables were treated as having normally distributed errors, and comprised each available colour band.

3.1.5 Input data and priors

The fits were performed to the combined UBVJHK data set (six colour bands), and separately to the UgriJHK data set (seven colour bands). Each covered the wavelength range 0.36–2.16 Å. Missing (not available from the relevant photometric survey catalogue) or bad (as defined in Sections 2.2–2.4) data were given an error of $10^5$ mag to ensure it did not affect the fit. We treated the KEBC temperature ratio as an observable with distribution as described in Section 3.1.3, and used this to constrain the temperature of the secondary star from that of the primary. We assumed priors on the model as detailed in Table 1. Where no KIC $T_{\text{eff}}$ was available for an object, 5000 K was used as the prior mean for $T_1$. We tested the effect of the prior on $T_1$ by running 1000 of the binary systems with first a prior of 5000 K with standard deviation 2000 K, and secondly a prior of the KIC $T_{\text{eff}}$ with the same standard deviation, in each case with no extinction. The offset in the means of the $T_1$ distributions was 14 K, so no significant systematic effect is caused by the prior. The standard deviation of the difference between the two cases, excluding non-converged systems, is ~200 K, well within the errors we quote in Section 4.2. As such we conclude that the choice of this prior has no significant effect on the retrieved values. The ‘primary’ star of each system was chosen using the KEBC temperature ratios – these values were taken for the purposes of fitting, even when they were greater than unity. In the final catalogue, the primary star values have been set as the star with the dominant flux contribution, as calculated from the temperature and radius ratios of the model output.

3.2 Testing

The model was tested on a simulated distribution of 1000 binary systems, for both the UBVJHK and UgriJHK data sets. These systems were generated with separate distributions for each physical stellar parameter, as no complete unbiased distribution could be found for these parameters in binary stars. We used the distributions as laid out in Table 2 (with all values constrained to be above zero), which were designed to cover the expected parameter space for the Kepler mission EBs. The distribution of temperature ratio $T_2/T_1$ was taken as a Gaussian approximation to the distribution of the KEBC. Note that this form of test involves generating fake colours using the very model atmospheres and filter transmissions used to fit them. Also, while it involves realistic parameter values, these do not combine to represent ‘real’ stars. Hence, this is purely a test of information content in the used colour bands. No significant difference was seen between each data set, as expected from their similar colour bands and wavelength ranges.

Simulated colour bands were generated via integrating over the CK04 model atmospheres as detailed above. The MCMC was run for 50 000 iterations with a burn-in period of 20 000 iterations. No significant extinction was included in this test. The retrieved values of $T_1$, $T_2$, $R_1/D$ and $R_2/R_1$ as compared to their input values for each data set are shown in Figs 1–4. The agreement in all parameters except $R_2/R_1$ shows that 20 000 is a sufficient number of iterations to allow convergence for the majority of systems. To remove as many as possible of those few remaining unconverged, a higher number of iterations is specified for the real data. The retrieval of surface gravity and metallicity was extremely poor. These parameters have very little impact on the observed colours within their error. As such these parameters were not included in the model. As shown above, the combination $R_2/D$ replaces $R_1$ and $D$ in the actual model run, as the latter two were not individually constrained.

For two stars with well separated temperatures it should be possible to fit each stellar atmosphere, and hence obtain information on both stellar temperatures and also the ratio of the radii of the stars (to each other and to the system distance). For the systems in the KEBC, however, the two stellar temperatures in general proved to be too close to allow this, as the peak emission of each star is often located too close in wavelength to that of the other star. This led to the well-retrieved information being in general the primary star temperature $T_1$ (and through the temperature ratio the secondary temperature $T_2$) along with a combination of parameters which we term the binary solid angle, equal to $(R_1^2 + R_2^2)/D^2$. The

| Parameter | Distribution | Parameters | Standard deviation | Lower limit | Upper limit |
|-----------|--------------|------------|--------------------|-------------|-------------|
| $T_1$     | Normal       | KIC $T_{\text{eff}}$ | 2000 K             | 3500 K      | 13 000 K (see Section 4.1) |
| $T_2/T_1$ | See Section 3.1.3 |           |                    |             |             |
| $R_1/D$   | Normal       | 0.003 $R_\odot$ pc$^{-1}$ | 0.05 $R_\odot$ pc$^{-1}$ | $10^{-5} R_\odot$ pc$^{-1}$ | $0.2 R_\odot$ pc$^{-1}$ |
| $R_2/R_1$ | Normal       | 0.8        | 0.3                | 0.01        | 3.0         |

Table 1. Model priors.

| Parameter | Distribution | Parameters | Standard deviation | Lower limit | Upper limit |
|-----------|--------------|------------|--------------------|-------------|-------------|
| $T_1$     | Uniform      | 3500 K     | 10 000 K           |             |             |
| $T_2/T_1$ | Normal       | 0.9123     | 0.1668             |             |             |
| $R_1$     | Normal       | 0.8 $R_\odot$   | 0.2 $R_\odot$     |             |             |
| $D$       | Uniform      | 50 pc      | 1500 pc            |             |             |
| $R_2/R_1$ | Normal       | 1.0        | 0.4                |             |             |
| log $R_1$ | Normal       | 4.5 cgs    | 0.2 cgs            |             |             |
| log $R_2$ | Normal       | 4.5 cgs    | 0.2 cgs            |             |             |
| $[M/H]$   | Uniform      | −2.5       | 0.5                |             |             |
| $A_V$     | Normal       | 0.05 mag   | 0.02 mag           |             |             |

Table 2. Distribution of test parameters.
Input and MCMC fit primary star temperatures \( T_1 \) for 1000 simulated sets of stellar parameters. The dashed line shows a perfect match. Dots represent the UBVJHK data set and crosses the UgriJHK. The small number of systems highly deviant from the dashed line have not converged.

Figure 2. As Fig. 1 for \( T_2 \).

Figure 3. As Fig. 1 for \( R_1/D \).

Figure 4. As Fig. 1 for \( R_2/R_1 \).

Figure 5. The dependence of \( R_2/R_1 \) fit quality on \( T_2/T_1 \). The 1000 simulated sets of parameters used in Fig. 1 plus 1000 additional sets with lower temperature ratios are shown.

4 RESULTS

4.1 Fitting parameters

Each object was run through the MCMC for 100 000 iterations, including a burn in period of 30 000 iterations (significantly more relevance of the binary solid angle as opposed to \( R_1/D \) and \( R_2/R_1 \) depends on the temperature ratio. For ratios significantly different from unity, the individual components \( R_1/D \) and \( R_2/R_1 \) become well retrieved. The difference between input and MCMC fit values for \( R_2/R_1 \) using the UBVJHK colours is shown as a function of \( T_2/T_1 \) in Fig. 5 (with an additional 1000 systems with lower temperature ratios added to illustrate the correlation). Note the systematic offset of about \(-0.2\) even at lower values of \( T_2/T_1 \). In what follows, we publish both \( R_1/D \) and \( R_2/R_1 \), as each is in some cases accurate, but users should note the above in choosing whether to use these values individually or combined into the binary solid angle mentioned. The relevance of \( R_2/R_1 \) should be determined from Fig. 5 in line with the needs of the user. We note that when \( T_2/T_1 \) approaches unity that for main-sequence stars \( R_2/R_1 \) should also be close to unity.
than was used in the test of Section 3.2). At 250 iteration intervals through the burn in phase, the model was tuned. Objects with KIC \( T_{\text{eff}} \leq 9000 \) K were run using a high temperature limit of \( 13,000 \) K for efficiency. Other objects (including those with no KIC value for \( T_{\text{eff}} \)) were run with a limit of \( 50,000 \) K, and are flagged in the catalogue.

In forming final values for each object, output parameters were checked for consistency between both data sets, and also between duplicate or triplicate UgriJHK data sets where available. We used \( T_1 \) as the parameter for checks (with \( T_1 \) defined as the temperature of the star dominating the system flux), as this was the strongest recovered parameter while testing. First, all fits with three or less bands were excluded. Then, in the cases where more than one fit was available, each fit was checked against each of the others to see if it was within \( 3\sigma \) (using the maximum \( \sigma \) of the two fits being checked). If the fits were thus consistent, they were both included in the weighted average (using their MCMC derived errors) to calculate the final set of values. This process was repeated for all possible fit combinations (the maximum number of fits for a system is four, one UBVJHK and three UgriJHK). In this way, highly deviant fits (for example due to bad photometric data) can be excluded from the final values where possible. For systems where no good fits were present, final values were formed using the weighted average of all available fits, and errors by the standard deviation of those fit values. These systems are flagged in the catalogue to highlight the systematic difference between their fits and/or the lack of photometry available.

### 4.2 Errors

We use the MCMC derived errors to represent the Gaussian noise associated with our model fitting. These have median values of \( 120 \) K for \( T_1 \), \( 310 \) K for \( T_2 \), \( 8.2e-5 \) R_{\odot} pc^{-1} for \( R_1/D \) and \( 0.17 \) for \( R_2/R_1 \). We also estimate the effect of extinction on the presented values, as the KIC extinctions are known to have particularly high error. We compare a run of the model on the UBVJHK data set with the KIC extinction values (as in the final run) and with no extinction. The error on the KIC extinction values (\( \sim 0.3 \)) is of the order of the values themselves (mean \( \sim 0.4 \)), so the difference in model fits generated by removing extinction represents a reasonable estimate of the error they could cause. We found that there was a median difference between fits with and without extinction of 350 and \( 540 \) K for \( T_1 \) and \( T_2 \), \( 7.3e-5 \) R_{\odot} pc^{-1} for \( R_1/D \) and for \( R_2/R_1 \) 0.15. As such, extinction has a significant effect. We treat these median extinction effects as a 1\( \sigma \) additional Gaussian error on the presented values, and give the combined error in the catalogue. While this is an estimate, neither the KIC extinction values nor their errors are characterized enough for a more detailed approach to be meaningful.

We note that this error estimation does not take into account of systematic offsets caused by contamination (‘third light’), bad data or bad extinction values, and objects affected will have larger errors. While we removed bad or contaminated photometric data where it was labelled as such, and applied errors to the input temperature ratios to reduce the impact of bad values, these issues will remain for some objects.

We then adopt 1\( \sigma \) errors formed from a combination of the effect of the extinction systematic and fitting noise values. Errors are presented individually for each system, but to give a guideline the median catalogue error is \( 370 \) K in \( T_1 \), \( 620 \) K in \( T_2 \), \( 2.5e-12 \) in \( R_1/D \) and \( 0.23 \) in \( R_2/R_1 \). For high temperatures (\( >9000 \) K), the errors on the temperature are larger, as seen in Fig. 1) and discussed in Section 5.2. The errors on the radius parameters will vary with \( T_2/T_1 \), as described in Sections 3.2 and 5.2. The derived temperature errors are consistent with the temperatures of various systems in the KEBC which have been studied in detail, see Section 5 for detail.

### 4.3 Catalogue

The format of our results is presented in Table 3 (the full catalogue available online as Supporting Information). For each object the results are given for each fitted data set, along with ‘final’ values. These are formed from the average of the available ‘good’ fits – fits can be excluded as explained in Section 4.1. Entries are flagged for various reasons; a summary of the used flags, in order in which they appear in the catalogue, is given in Table 4.

#### Table 3. Catalogue Format. UBV = UBVJHK, KIS = UgriJHK.

| Column header | Description | Column header | Description |
|---------------|-------------|---------------|-------------|
| KIC ID        | Kepler Input Catalogue identifier | \( T_2 \) \( KIS_1 \), Error | \( -1 \) if None |
| \( T_1 \) Final, Error | Final primary temperature and error (K) | \( R_1/D \) \( KIS_1 \), Error | \( -1 \) if None |
| \( T_2 \) Final, Error | Final secondary temperature and error (K) | \( R_2/R_1 \) \( KIS_1 \), Error | \( -1 \) if None |
| \( R_1/D \) Final, Error | Primary radius/system distance and error | \( KIS_1 \) Bands Used | \( 1 \) if used, order \( -- \) UgriJHK |
| \( R_2/R_1 \) Final, Error | Component radii ratio and error | \( T_1 \) \( KIS_2 \), Error | \( -1 \) if None |
| \( T_2/T_1 \) Input | Input prior temperature ratio | \( T_2 \) \( KIS_2 \), Error | \( -1 \) if None |
| Flags | Four digit flag of fit quality, see Table 4 | \( R_1/D \) \( KIS_2 \), Error | \( -1 \) if None |
| Output Source | Final values source, UBV, KIS1, KIS2, KIS3, 1 if used | \( R_2/R_1 \) \( KIS_2 \), Error | \( -1 \) if None |
| \( T_1 \) UBV, Error | \( -1 \) if None | \( KIS_1 \) Bands Used | \( 1 \) if used, order \( -- \) UgriJHK |
| \( T_2 \) UBV, Error | \( -1 \) if None | \( T_1 \) \( KIS_3 \), Error | \( -1 \) if None |
| \( R_1/D \) UBV, Error | \( -1 \) if None | \( T_2 \) \( KIS_3 \), Error | \( -1 \) if None |
| \( R_2/R_1 \) UBV, Error | \( -1 \) if None | \( R_1/D \) \( KIS_3 \), Error | \( -1 \) if None |
| UBV Bands Used | 1 if used, order UBV--JHK | \( R_2/R_1 \) \( KIS_3 \), Error | \( -1 \) if None |
| \( T_1 \) \( KIS_1 \), Error | \( -1 \) if None | \( KIS_2 \) Bands Used | \( 1 \) if used, order \( -- \) UgriJHK |
| \( T_2 \) \( KIS_2 \), Error | \( -1 \) if None | \( KIS_3 \) Bands Used | \( 1 \) if used, order \( -- \) UgriJHK |

#### Table 4. Catalogue flags.

| Column | Flag description |
|--------|------------------|
| 1      | 1 if object run with 50 000 K temperature limit |
| 2      | 1 if no KIC \( T_{\text{eff}} \), \( A_v \) or log \( g \) values available |
| 3      | 1 if candidate or proven three-body system |
| 4      | 1 if no KEBC eclipse information available |
| 5      | 1 if no matching fits available with 4+ colour bands |
4.4 Distributions

We form distributions of our output parameters using the ‘final’ values as detailed in the results catalogue. Systems for which no good final value could be formed were discarded (this left 2457 of the original 2610 systems, in at least one data set). While the $R_1/D$ distribution is generally uninformative due to the unknown distance, the $T_1$ and $T_2$ distributions, and in combination the $T_2/T_1$ distribution, is worth noting. The $R_2/R_1$ distribution is in general poorly fit so is again uninformative. The results for $T_1$ and $T_2$ are shown in Figs 6 and 7. In presenting the temperature ratio, we show the total distribution (Fig. 8), and also the distribution split by stellar spectral type. We show the results for ‘cool’ ($T_1 < 5200$ K, roughly K and M stars), solar type ($5200 \leq T_1 < 7500$ K, roughly F and G stars) and ‘hot’ ($T_1 > = 7500$ K, roughly A stars). These are presented normalized to their sample sizes in Figs 9–11, and are discussed in Section 5.

It is also worth comparing our results to the KIC itself. Assuming a single star as the KIC does will tend to focus on the primary star as the dominant source of flux. As such we compare the KIC $T_{\text{eff}}$ to our $T_1$ in Fig. 12. A general trend of an increase in our temperatures over the KIC’s can be seen – this is expected, as in each of these systems an extra contribution from a usually cooler star has been included. The effect of our increased temperature limit over the KIC is also notable.

5 DISCUSSION

5.1 Overview

We have applied a two-stellar-component MCMC model to the EB stars of the KEBC, using a larger wavelength range than that previously utilized by the KIC. In particular, we add the $U$ band, in principle improving our results for hotter stars. We find that the useful results of our model are the effective temperatures of both stars, as well as the parameters $R_1/D$ and $R_2/R_1$. For values of $T_2/T_1$ close to unity, these parameters are not individually fitted and the combination $(R_1^2 + R_2^2)/D^2$ is instead. The errors on these parameters were found to be on average 370 K in $T_1$, 620 K in $T_2$, $2.5e−12$
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Figure 10. The normalized distribution of $T_2/T_1$ for stars cooler than 5200 K, total number 303.

Figure 11. The normalized distribution of $T_2/T_1$ for stars hotter than 7500 K, total number 246.

Figure 12. Comparison of KIC $T_{\text{eff}}$ and final catalogue $T_1$ values. The dashed line represents a 1:1 match. The difference arises from the inclusion of two stars in our model as compared to the single star of the KIC, and also our higher temperature limit.

in $R_1/D$ and 0.23 in $R_2/R_1$. We anticipate that this catalogue will be of use in target selection of Kepler EB stars, approximation of parameters and to generally inform anyone wishing to make use of these objects’ extremely high-precision light curves. We note that these results use temperature ratios derived from the eclipse depth measurements of the KEBC, and as such they rely on that catalogue to that extent. While the primary star temperatures will only be slightly affected by a largely erroneous temperature ratio, the secondary star temperatures are more sensitive.

5.2 Shortcomings

There are various issues involved in the production of this catalogue, the worst of which we summarize here. Some of these issues are in common with those of the KIC (Brown et al. 2011).

5.2.1 High/low $T$

The CK04 stellar atmospheres which we use have a lower limit of 3500 K. As such, temperatures which lie close to this value ($T < 3750$ K) should not be taken as accurate. In terms of selecting cool stars however they can be used – while the temperature is not accurate, any object with a catalogue temperature around this level is unambiguously cool. At high temperatures ($T > 9000$ K), a large systematic effect, visible in Fig. 1, means that our temperatures have much higher errors, and are likely underestimated. Again, these are still hot stars, but the exact temperature values should not be trusted.

5.2.2 Binary solid angle versus $R_1/D$ and $R_2/R_1$

As described in Section 3.2, the $R_1/D$ and $R_2/R_1$ values are generally poorly constrained. This is because for most of the systems in the KEBC, the temperatures of the two stars are close enough that little information is contained on the secondary star’s relative contribution to the flux. Fig. 5 shows that only systems with $T_2/T_1 \leq 0.6$ constrain $R_1/D$ and $R_2/R_1$, and in these cases there is still a systematic underestimate of $\sim 0.2$ in $R_2/R_1$ which has not been adjusted for. In the other systems, which represent the majority of those here, the binary solid angle, equal to $(R_1 + R_2)^2/D^2$ and representing a combined measure of the level of flux incoming at the Earth is constrained instead, and can be recovered from the catalogue values as $(R_1/D)^2(1 + (R_2/R_1)^2)$.

5.2.3 Contamination

As has been mentioned previously, our model assumes only two stellar components, and does not take account of additional sources of flux. The proportion of KEBC objects with additional companions is $\sim 20$ per cent (Rappaport et al. 2013), meaning they represent a significant part of our catalogue. We have removed data flagged as contaminated in the various photometric surveys used, and marked objects which are confirmed as or possible 3+ body systems (Carter et al. 2011; Derekas et al. 2011; Gies et al. 2012; Conroy et al. 2013; Rappaport et al. 2013). These systems can still be of use – for example, KIC5897826 is a triple star and is tested successfully against our two-star model in Table 5. In cases, where more than two stellar components are present in a system, the derived physical properties will be affected to the extent that the extra companions contribute to the flux.
5.2.4 Extinction and reddening

Our use of the KIC $A_V$ values allows us to reduce our already large parameter space while still using reasonable extinction values. Attempts to fit these values ourselves were very poorly constrained. Extinction is not generally well constrained – typical errors on the KIC $E(B-V)$ values are of 0.1 mag, implying a 0.31 mag typical error on $A_V$ (Brown et al. 2011), which is of the order of the $A_V$ values. The KIC paper itself notes the problems involved in its extinction parameters, including no account of small-scale structure in the interstellar extinction. These errors are incorporated here, and will affect the systems in our catalogue. We have attempted to include the systematic effects of bad extinction in our errors (see Section 4.2), but users should be aware that anomalously high extinctions will produce too high temperatures, and the reverse for low extinctions.

5.3 Distributions

While our individual stellar temperatures are not constrained by spectroscopy, and so have a larger potential for biases and non-physical effects to show themselves, they offer a particularly large sample size – 303 cool stars, 1908 solar type and 246 hot stars. However, as the stars under consideration are drawn from an unconstrained sample of ages (and the expected stellar temperature varies with evolution), the temperature distributions are generally uninformative by themselves. The temperature ratio distributions split by spectral type show slight differences, however, due to the lower number of samples in each bin of the cool and hot distributions there is not a strong case for any statistically significant difference. This implies that systematic effects in the fitting of different temperature stars were not strong, supporting the robustness of our results across the different temperature regimes. All of the presented distributions have potential biases present, in the effect of the particular combination of colour bands which we utilize, as a residual effect of the KEBC recovery of eclipse depths, or as a sampling effect in the eclipsing binaries which Kepler selects.

5.4 Performance on known objects

A limited number of these EB systems, analysed in depth for other reasons, are available to compare with our results. While this sample is far from ideal (by definition these are systems which were selected as ‘interesting’ for a variety of reasons, and hence unlikely to be typical) we would still hope to predict their temperatures reasonably well. We found 11 systems where detailed analysis had been done. Five of these represent interesting stellar objects (e.g. sdB+white dwarves, triple systems), whereas the other six were circumbinary planet hosts. In the stellar cases, the primary star often dominates the flux, and in these circumstances we would expect to fit this star reasonably well. The spectroscopically derived individual temperatures are compared to ours in Table 5. We chose to contain our comparison to temperatures, as in the majority of cases no distance information is available. Encouragingly, both the primary and secondary temperatures fit well, within the errors we derive. For the three hot star entries in the table, the fits are generally worse, in all cases lying outside 3σ for at least one star. They are however, unambiguously high, representing some of the highest temperatures in our catalogue. This highlights that while we can select ‘hot’ stars reasonably well, precise temperatures at values greater than ~9000 K can have larger errors. This does not affect the selection of ‘hot’ stars used in the above distributions.

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APPENDIX A: GENERATION OF $T_2/T_1$

A1 Known parameters

The KEBC provides periods for each of the binary systems, as well as eclipse depths and measurements in phase of eclipse durations and separations. We produced eccentricity and argument of periapsis ($\omega$) measurements using these durations and separations, through the formulae of Kalrath & Milone (2009). Initial values of $T_2/T_1$ were produced directly from the ratio of eclipse depths. In some cases, no eclipse depth ratio or phase measurements were available, usually due to non-detection of the secondary eclipse.

A2 Measurement scatter

This was taken to be a Gaussian error of 0.025 and 0.05 for over contact and non-overcontact binaries, respectively, from the test figs 8 and 10 of Prsa et al. (2011). Overcontact systems were defined as having morphology parameter greater than 0.7 (see Matijević et al. 2012). While these numbers come from older versions of the KEBC, they represent a reasonable estimate of the uncertainty in recovering $T_2/T_1$ from EB light curves.

A3 Eccentricity correction

This arises from the possibility of different surface areas being occulted in primary and secondary eclipse. The ratio of areas acts as a correction to the temperature ratio, in the form

$$\frac{T_2}{T_1} = \frac{A_1}{A_2} \left( \frac{D_1}{D_1} \right)^{1/4},$$

where $D$ represents an eclipse depth and $A$ the stellar surface area occulted in eclipse. The area eclipsed can be calculated from equation 1 of Mandel & Agol (2002), and is a function of the projected orbital separation at eclipse, plus the stellar radius. The projected orbital separation at eclipse is then itself a function of period, eccentricity, argument of periapsis, system mass and inclination. This leaves the radii, mass and inclination unknown. We estimated the possible effect of this correction by drawing 10,000 random sample binaries for each KEBC binary, with primary radii drawn uniformly between 0.2 and 1.56 $R_\odot$, 1.56 $R_\odot$ is the Torres, Andersen & Giménez (2010) radius of a $T = 12,000$ K star with surface gravity 4.5 and 0.02 metallicity, chosen as an upper limit as the majority of our catalogue lie below this temperature. Secondary radii were drawn uniformly between 0.2 and the primary radius. Inclinations were constrained such that both stars eclipse. Given these radii, masses were found from the zero-age main sequence, solar metallicity models of Girardi et al. (2000).

The area correction was calculated for each sample, and applied to equation (A1), giving a distribution of $T_2/T_1$. We found this to be of the form

$$P \left( \frac{T_2}{T_1} \right) \propto \gamma \delta(\mu)
+\left(1 - \gamma \right) \left( \alpha_1 e^{\beta_1 \frac{|\mu - \mu_1|}{\pi}} + \alpha_2 e^{\beta_2 \frac{|\mu - \mu_2|}{\pi}} \right),$$

where $\mu$ represents the initial value of $T_2/T_1$, produced from equation (A1) with $A_1/A_2$ set to unity. This consists of two components, a delta function at $\mu$ (from the samples where both eclipses were total, leading to zero correction), and a continuous distribution which we found to be best fitted by a sum of exponentials. The remaining parameters of equation (A2) were found for each KEBC binary. We limit ourselves to this first order treatment of the eccentricity effect, ignoring limb darkening and starspots, which are both poorly constrained here.

A4 Combined $T_2/T_1$ distribution

The above inputs were combined into a final distribution of $T_2/T_1$, suitable for input as a prior into the MCMC. This distribution is found by convolving the measurement and eccentricity correction terms. For simplicity, we convolved the measurement Gaussian with the delta function component of the eccentricity correction only. This is equivalent to approximating the exponential terms to dominate outside of approximately one Gaussian standard deviation. This led to a final $T_2/T_1$ distribution of the form

$$P \left( \frac{T_2}{T_1} \right) = \frac{1}{N} \left( \gamma N(\mu, \sigma)
+\left(1 - \gamma \right) \left( \alpha_1 e^{\beta_1 \frac{|\mu - \mu_1|}{\pi}} + \alpha_2 e^{\beta_2 \frac{|\mu - \mu_2|}{\pi}} \right) \right),$$

where $N$ is a normalization constant and $\sigma$ is set as described in Section A2. In cases where no eclipse depth ratio or duration information was available, we set the prior on $T_2/T_1$ to be a Gaussian with mean 0.7 and standard deviation 0.5, representing a very weak constraint.

SUPPORTING INFORMATION

Additional Supporting Information may be found in the online version of this article:

Table 3. Catalogue of stellar parameters, as described by Table 4 (http://mnras.oxfordjournals.org/lookup/suppl/doi:10.1093/mnras/stt2146/-/DC1).

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