Running with \textit{BICEP}2: Implications for Small-Scale Problems in CDM

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\textbf{ABSTRACT}

The \textit{BICEP}2 results, when interpreted as a gravitational wave signal and combined with other CMB data, suggest a roll-off in power towards small scales in the primordial matter power spectrum. Among the simplest possibilities is a running of the spectral index. Here we show that the preferred level of running alleviates small-scale issues within the ΛCDM model, more so even than viable WDM models. We use cosmological zoom-in simulations of a Milky Way-size halo along with full-box simulations to compare predictions among four separate cosmologies: a \textit{BICEP}2-inspired running index model ($\alpha_s = -0.024$), two fixed-tilt ΛCDM models motivated by \textit{Planck}, and a 2.6 keV thermal WDM model. We find that the running \textit{BICEP}2 model reduces the central densities of large dwarf-size halos ($V_{\text{max}} \sim 30 - 80\, \text{km}\,\text{s}^{-1}$) and alleviates the too-big-to-fail problem significantly compared to our adopted \textit{Planck} and WDM cases. Further, the \textit{BICEP}2 model suppresses the count of small subhalos by $\sim 50\%$ relative to \textit{Planck} models, and yields a significantly lower “boost” factor for dark matter annihilation signals. Our findings highlight the need to understand the shape of the primordial power spectrum in order to correctly interpret small-scale data.

\textbf{Key words:} dark matter – cosmology: theory – galaxies: halos – Local Group

1 INTRODUCTION

The discovery of the cosmic microwave background (CMB) and measurements of its temperature anisotropy have lead to a standard cosmological model consisting of a flat universe dominated by cold dark matter and a cosmological constant that drives accelerated expansion at late times (e.g., \textit{Planck} Collaboration et al., 2013). Inflation extends this standard cosmology by positing an earlier period of rapid exponential expansion that sets the initial conditions for the hot big bang; this period alleviates a number of “fine-tuning” problems, but lacked supporting observational evidence. Recently, however, the \textit{BICEP}2 experiment reported the detection of primordial B-modes in the CMB (\textit{BICEP}2 Collaboration et al., 2014). One explanation for this signal is the stochastic background of gravitational waves generated by inflation, providing potentially the first direct evidence for an inflationary phase in the early Universe. This explanation will have to be verified by other experiments and in other frequencies. For the rest of this paper, we will assume this explanation is correct as we await confirmation by other experiments and in other frequency bands.\footnote{In this regard, note that there has been concern that foreground contamination could have affected this measurement (e.g., Liu et al., 2013).}

The tensor-to-scalar ratio measured by \textit{BICEP}2, $r = 0.20^{+0.07}_{-0.05}$ (68\% confidence-interval), is at face value inconsistent with the limit quoted from a combination of \textit{Planck} (\textit{Planck} Collaboration et al., 2013; Ade et al., 2013), \textit{SPT} (Hou et al., 2014), \textit{ACT} (Das et al., 2014), and \textit{WMAP} polarization (Hinshaw et al., 2013) data: $r < 0.11$ at 95\% confidence. However, these pre-\textit{BICEP}2 limits assumed a constant spectral index $n_s$ for scalar fluctuations in the primordial power spectrum. The discrepancy could be explained by a nontrivial primordial power spectrum, one that deviates from a pure power law (e.g., Hazra et al., 2014); suppressing the large-scale scalar power spectrum relative to that

\begin{itemize}
  \item [\footnote{As noted by Audren et al., 2014, however, the measured tension may be significantly reduced ($\sim 1.3\sigma$) by assuming identical values for the pivot scale and the tensor spectral index in both analyses, effectively raising the upper limits on the running measured by \textit{Planck}.}]
\end{itemize}
expected in a constant spectral index model allows for a larger contribution from tensor modes to the temperature-temperature anisotropy $C_{TT}$ at large scales. Abazajian et al. (2014) explored several scenarios including a running spectral index, a cutoff in the spectrum, and a break in the power spectrum, finding evidence for a negative running index (see also McDonald 2014; Ashoorioon et al., 2014) or for a broken spectrum. Of these possibilities, the running spectral index is arguably the simplest, and we focus on the small-scale implications of this solution for the remainder of this work. More generally, however, our results explore the possible implications of non-trivial primordial power spectra on galaxy formation. Here we specifically show that viable deviations from power-law primordial power spectrum can have a significant impact on important questions facing $\Lambda$CDM today.

Any modifications to the primordial power spectrum and cosmological parameters will manifest itself in the formation and evolution of large-scale structure. On large scales, the standard $\Lambda$CDM cosmology provides an excellent model for the observed Universe (Ho et al., 2012; Henshaw et al., 2013); any changes that compromise this success would thus be a sign of an inconsistent scenario.

On the other hand, discrepancies currently exist between the $\Lambda$CDM paradigm and the observed Universe on smaller scales. Examples include the “core/cusp problem,” where dissipationless N-body simulations in $\Lambda$CDM predict a rising dark matter density with smaller radius $\rho \propto r^{-1}$, in contrast to observations that show a core-like profile at small radii (Flores & Primack, 1994; Moore et al., 1999). The discrepancy is seen in low-surface brightness (LSB) galaxies (Simon et al., 2005; Donato et al., 2009; de Naray & Kaufmann, 2011; Oh et al., 2011), but also seems to appear in lower luminosity dwarf spheroidal (dSph) galaxies. The second discrepancy is that the count of known satellite galaxies around the Milky Way is much smaller than the count of subhalos expected to be massive enough to form stars (Klypin et al., 1999; Moore et al., 1999) the “missing satellites problem”). Independently, it has also been shown that the central densities of dSphs are significantly lower than predicted by dissipationless $\Lambda$CDM simulations, dubbed the “too-big-to-fail problem” (TBTF; Boylan-Kolchin et al., 2011, 2012). The severity of TBTF remains an active debate in the literature, with some authors pointing out that a reduced MW mass would effectively eliminate the problematic halos (e.g. Wang et al., 2012; Cautun et al., 2014) and others arguing that baryonic processes, such as reionization, supernova feedback, tidal interactions, and ram pressure stripping, may reduce the central densities of simulated dwarf halos (e.g. Bullock et al., 2000; Somerville, 2002; Pontzen & Governato, 2012; Zolotov et al., 2012; Brooks & Zolotov, 2013; Arraki et al., 2013; Gritschneder & Lin, 2013; Garrison-Kimmel et al., 2013; Amorisco et al., 2014; Del Popolo et al., 2014; Sawala et al., 2014; Pontzen & Governato, 2014).

Quantitatively, the magnitude of these small-scale problems and the degree to which feedback and other baryonic processes can operate to solve them depend on the underlying power spectrum and cosmological parameters, which fundamentally affect the collapse times and central densities of dark matter halos. For example, Zentner & Bullock (2002, 2003) showed that non-trivial primordial power spectra of the type expected in basic inflation models can alleviate many of the small-scale problems faced by $\Lambda$CDM, and used semi-analytic models to show that running at the level of $\alpha_s \sim -0.03$ can reduce discrepancies significantly. Later, using numerical simulations, Polisensky & Ricotti (2014) showed that differences in best-fit $\sigma_8$ and $n_s$ values between WMAP data releases impact small-scale predictions in important ways. The implication is that changes that follow from the BICEP2 results can affect the magnitude of small-scale discrepancies significantly. Similarly, imposing a free-streaming cutoff in the initial power spectrum (e.g. from warm dark matter, WDM, or from a non-trivial inflation model) may also aid in resolving problems (Kamionkowski & Liddle, 2000; Zentner & Bullock, 2003; Kaplinghat, 2005; Lovell et al., 2014; Schneider et al., 2014). Specifically, WDM with a thermal mass of 2 keV has been shown to be sufficient to solve some of the problems (Anderhalden et al., 2013). Although this mass is in conflict with existing limits on free-streaming cutoffs (e.g. Polisensky & Ricotti, 2011; Viel et al., 2013; Schneider et al., 2014), the limits are subject to systematic uncertainties, and more robust limits based on phase-space arguments and subhalo counting are just below 2 keV (Boyarsky et al., 2009; Gorbunov et al., 2008; Horiuchi et al., 2014).

The BICEP2 measurement may also have interesting consequences on searches for potential annihilation signals from dark matter itself (indirect detection studies). The annihilation signal from a single halo scales as the square of the dark matter density, $\rho_{DM}$, but otherwise the boost factor, the contribution to the expected annihilation signal due to substructure, is dependent on the slope and normalization of the substructure mass function. Reducing any of these quantities could significantly loosen the upper limits placed by the searches that employ substructure boost (Kamionkowski et al., 2010; Anderson et al., 2010; Sánchez-Conde & Prada, 2014; Ng et al., 2014).

In this paper, we investigate the impact of the running power spectrum on structure formation in the Universe by simulating the evolution of a MW-size host in four separate cosmologies: the model motivated by BICEP2, the Planck cosmological model, a WDM model with the Planck parameter set, and a flat universe with a lowered $\Omega_{m}$ but otherwise identical to the Planck universe in order to control for the difference in $\Omega_{m}$ between the Planck and BICEP2 models.

This paper is organized as follows: §2 describes the simulations, including the cosmological models that we compare; §3 presents our results for the cosmological mass function at $z = 3$, the subhalo $V_{max}$ function of a MW-size host at $z = 0$, and discuss the changes in the internal kinematics of the highest mass subhalos (the TBTF problem) as well as implications for the substructure boost; we summarize our findings in §4.
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2 SIMULATIONS AND ANALYSIS

We have run collisionless, dark matter-only simulations of a 50h^{-1} Mpc periodic region with the Tree-PM code Gadget-3 [Springel, 2005], beginning at z = 125. We present seven simulations, three of which model the full volume at medium resolution (n_s = 1024^3) and four of which are “zoom-in” simulations aimed at a Milky Way (MW)-size host. Initial conditions were created with MUSIC [Hahn & Abel, 2011]. We include the running in the BICEP2 universe by defining

$$T^2(k) = \left(\frac{k}{k_s}\right)^{\alpha_s} T^2(k_s),$$

where $\alpha_s = \frac{dn_s}{dk} \ln \left(\frac{k}{k_s}\right)$ is the running of the spectral index, $k_s = 0.05$ Mpc^{-1} [Abazajian et al., 2014], and $T(k)$ is the standard definition of the transfer function. We pass $T^2(k)$ to MUSIC as the transfer function.

We list the four underlying cosmological models that we adopt in Table 1. For the BICEP2 universe, we select the “running” model from [Abazajian et al., 2014], who performed a joint Bayesian analysis on the BICEP2 B-mode polarization data and the temperature and lensing data from Planck Collaboration et al. (2013); those parameters are listed in the first column. We elect to compare this model to that suggested by the Planck temperature power spectrum data alone (Table 2, Column 2 of Planck Collaboration et al. 2013), reproduced in the second column. We additionally simulate structure formation in two Planck-like control models, Low-$\Omega_M$ and WDM_2.6keV. Both adopt the majority of the Planck parameters, but Low-$\Omega_M$ artificially lowers the overall matter density, $\Omega_M$, to $\sim 3\sigma$ below that suggested by Abazajian et al. (2014), while maintaining flatness in order to control for the lowered $\Omega_M$ in the BICEP2 cosmology. The WDM_2.6keV cosmology is identical to the Planck model, but imposes a relativistic free-streaming cut-off in the power spectrum for a thermal WDM particle equivalent mass of $m_{\text{WDM}} = 2.6$ keV. The mass is chosen to obey the robust limits from phase-space arguments of MW dSphs galaxies and strict counting of M31 satellites [Horiuchi et al., 2014], and is also marginally consistent with measurements of the Ly-$\alpha$ at 3$\sigma$ [Viel et al., 2013]. A WDM particle mass of 2 keV has been shown to solve small-scale issues in CDM [Anderhalden et al., 2013], but we opt for a slightly more massive particle in order to explore a value distinct from others.

The initial (z = 125) matter power spectra for these cosmologies are shown in Figure 1. The upper panel plots $k^3P(k)$ for the BICEP2 parameters in black, the Planck model in cyan, and the Low-$\Omega_M$ and WDM_2.6keV control models in magenta and yellow, respectively. The ratio of each model, relative to the Planck power spectrum is plotted in the lower panel. The light-grey region indicates the scales that are currently probed by the Lyman-$\alpha$ forest (50h^{-1} Mpc $\sim 50$ Mpc; [Viel et al., 2013]) and the dark grey region indicates the mass ranges of interest to dwarf galaxy formation ($M_{\text{halo}} \sim 10^9 - 10^{11} M_\odot$); the darkest overlap region roughly corresponds to the mass scales of $V_{\text{max}} \sim 35$ km s^{-1} halos, which are characteristic of the problematic halos identified in TBTF.

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spectrum differs from that of Planck by as much as ~ 30% at the scales probed by the Ly-α forest; studies of the Ly-α forest power spectrum are sensitive to running, and the most recent results have found values consistent with the running we adopt here $\alpha_s = -0.028 \pm 0.018$ [Lesgourgues et al. 2007]. The $\gtrsim 30\%$ reduction in the primordial power at the smaller scales associated with the formation of dwarf halos, however, has interesting consequences for the small-scale problems discussed above. The unlabeled region to the right of dwarf scales are associated with so-called “mini-halos,” which may be probed by gravitational lensing studies (e.g., Keeton & Moustakas, 2009) or tidal stream analyses (Ngan & Carlberg 2014). This range is also important for the overall “boost” factor due to dark matter annihilation in substructure (Sánchez-Conde & Prada, 2014), indicating that the $\textit{BICEP2}$ power spectrum will likely produce a much smaller DM annihilation signal from these mini-halos.

We first compare the cosmologies by simulating the entire 50 h$^{-1}$ Mpc volume at moderate resolution ($n_p = 1024^3$) until $z = 3$ with the Planck, Low-$\Omega_M$, and $\textit{BICEP2}$ cosmologies. The particle masses for these “full-box” simulations are given in Table 1 as $m_{p, FB}$ in units of $10^7 M_\odot$. We fix the Plummer-equivalent softening lengths of the full-box simulations at 5 comoving $h^{-1}$ kpc until $z = 9$, at which time they become 500 physical $h^{-1}$ pc. Dark matter structure is identified with the AMIGA Halo Finder (AHF, Knollmann & Knebe 2009), a publicly-available three-dimensional spherical overdensity halo finder. A slice of the simulation volume at $z = 3$ is shown in Figure 2 for the $\textit{BICEP2}$ cosmology (top) and the fiducial Planck model (bottom) – the two appear indistinguishable at these scales, though we will show below that there is a small systematic offset in the halo mass function, consistent with expectations from linear theory.

In order to study the highly non-linear regime, however, we primarily focus our efforts on “zoom-in” simulations [Katz & White 1993; Ögorbe et al. 2014] aimed at a MW-sized host, similar to the Via Lactea II [Diemand et al. 2008; Kuhlen et al. 2008] and Aquarius (Springel et al. 2008) projects. Specifically, we selected a highly isolated host from the ELVIS simulations (Garrison-Kimmel et al. 2014) and re-create the parent box, oversampling the region from which the halo forms with higher resolution, with the four underlying cosmological models given in Table 1. The zoom-in simulations are initialized with an effective resolution of $4096^3$ particles in the high resolution region. Similar to the full-box simulations, the softening lengths of these lowest mass particles is kept fixed at 1 comoving $h^{-1}$ kpc until $z = 9$, after which it is held fixed at 100 physical $h^{-1}$ pc until $z = 0$. The particle masses for each cosmological model are listed as $m_{p, HR}$ in Table 1 again in units of $10^7 h^{-1} M_\odot$. Each cosmological model was initialized with identical phases for the perturbations at all scales in order to reduce numerical differences (e.g., in the subhalo orbits) between the models. As in the full-box simulations, we search for collapsed structures in the $z = 0$ particle data with AHF. A visualization of a cube $500 h^{-1}$ kpc on a side, centered on the zoom-in target, is shown in Figure 3. The images are colored by the local matter density and show, from top left to bottom right, the BICEP2 simulation, the Planck model, the Low-$\Omega_M$ cosmology, and the WDM$_{2.6\text{keV}}$ model. The agreement between the Planck models, in spite of the free-streaming cutoff or shift in $\Omega_m$, is uncanny; the BICEP2 cosmology, however, has less overall substructure and clearly distinct orbits for the largest subhalos, indicative of the significant differences in power at $M \sim 10^9 - 10^{11} M_\odot$ scales seen in Figure 1.

Our zoom-in simulations are run with identical particle numbers, box sizes, and softening lengths (in $h^{-1}$ units) as the fiducial simulations in the ELVIS Suite (Garrison-Kimmel et al. 2014a); we therefore adopt the ELVIS resolution cut here and study only halos with maximum circular velocities $V_{\text{max}} > 8$ km s$^{-1}$. Similarly, Garrison-Kimmel et al. (2014b) showed that the relationship between $V_{\text{max}}$ and the radius at which $V_{\text{max}}$ occurs, $R_{\text{max}}$, is converged for halos larger than 15 km s$^{-1}$ and with $R_{\text{max}} > 0.36 h^{-1}$ kpc for simulations at this resolution; we again use the same criteria when examining the internal structure of small halos.

3 RESULTS

We begin by examining the halo mass function in the 50 $h^{-1}$ Mpc full-box runs at $z = 3$. Plotted as solid lines

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4 We do not simulate the volume with the WDM$_{2.6\text{keV}}$ cosmology as the model is designed to agree with our Planck run at the scales probed by such a simulation.

5 AHF is available at [http://popia.ft.uam.es/AHF/Download.html](http://popia.ft.uam.es/AHF/Download.html)

6 We also find identical results using the 6D friend-of-friends halo finder ROCKSTAR (Behroozi et al. 2013).
in the top panel of Figure 4 is the anti-cumulative number density of host halos, defined as those with their centers outside the virial volumes of all halos larger than itself, as a function of virial mass $M_v$; the lower panel plots the ratio of each line relative to the fiducial Planck model. The BICEP2 cosmology exhibits a suppression on all mass scales such that the Planck mass function is offset by $\sim 30\%$ at fixed number, though the offset rises slighter at lower masses, consistent with the running in the power spectrum. We note that presenting results in $M_\odot$ rather than $h^{-1} M_\odot$ would only increase the difference between the two simulations as the Planck cosmology adopts a smaller Hubble parameter.

This offset, however, is consistent with expectations from linear theory of structure collapse. Plotted as dashed lines in Figure 4 are the results of applying the analytical fitting function of Tinker et al. (2008)8. The ratios of these fitting functions are plotted as dashed lines in the lower panel. The Tinker et al. fit agrees nearly perfectly with our simulated mass functions, and the relative offsets from the Planck model are also in excellent agreement with the simulations.

We conclude that analytic mass functions based on linear theory may be used to make accurate predictions (at least until $z = 3$) in the BICEP2 cosmology.

Given that the differences in the primordial power spectrum increase with decreasing scales, we can expect to see even more extreme differences on the scales of dwarf galaxy halos. We therefore turn our analysis to the zoom-in simulations described in Section 2 which we exclusively use for the remainder of the work. The properties of the main host halo, given in Table 2 vary slightly between the four models; we therefore present subhalo counts as a function of $V_{v}\text{/}V_c$, where $V_c$ is the circular velocity of the host halo at the virial radius. This minimizes the halo-to-halo scatter and normalizes for the effects of varying host mass.

This normalized $V_{v}$ function is plotted in the top panel of Figure 5 for all four cosmological models; the lower panel again plots the ratio of each model to the Planck cosmology. The upper axis is scaled to $V_c = 160 \text{ km s}^{-1}$, roughly the virial velocity of a MW-size host and the mean $V_c$ of the host in the four simulations. When normalizing by $V_c$, the agreement between the Planck and Low-$\Omega_M$ models is nearly perfect at all $V_{v}$, even at the high $V_{v}$ end where small-number statistics typically dominate; if the counts are not normalized by the virial velocity, however, the Low-$\Omega_M$ model lies $\sim 25\%$ below the Planck cosmology at fixed subhalo $V_{v}$. The BICEP2 counts, however, are suppressed even after normalizing by $V_c$, particularly for subhalos less massive than $V_{v} \sim 30 \text{ km s}^{-1}$. The total count is $\sim 50\%$ below the Planck line at the resolution limit, alleviating the

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7 We use the term “virial radius” to refer to the radius at which the overdensity relative to the critical density drops to 173.8 (BICEP2), 174.3 (Planck), and 173.3 (Low-\Omega_M) at $z = 3$ and 99.8 (BICEP2), 104.1 (Planck), 96.5 (Low-\Omega_M), and 104.1 (WDM$_{2.66\text{keV}}$) at $z = 0$, and “virial mass” to refer to the total mass contained within that radius.

8 Theoretical mass functions are calculated via the publicly available code provided by Murray et al. (2013).
severity of the missing satellites problem. As expected, subhalos are even more strongly suppressed in the WDM\textsubscript{2.6keV} universe, with counts a factor of $\sim 6$ lower than the fiducial Planck model at the resolution limit. While this suppression drastically reduces the severity of the missing satellites problem, it may actually under-produce the required subhalo count compared to the known count of M31 satellites (e.g. Horiiuchi et al. 2014). The BICEP2 model has no such difficulties.

Due to the overall suppression of substructure in BICEP2 it is possible that counts of high mass ($V_{\text{max}} \sim 80$ km s\textsuperscript{-1}) satellites will provide an additional constraint on the running. While we do not see any significant differences in the few subhalos that exist in the simulated host at that mass range, it is possible that some reduction exists on a statistical level, particularly for close pairs. As Tollerud et al. (2011) showed that ΛCDM-like cosmologies reproduce observations reasonably well at Large Magellanic Cloud (LMC)-like masses, such counts may be used as a probe of the initial power spectrum in the future. Such a study, however, would require large simulations with higher resolution than those presented here, simulated until $z = 0$.

We now turn our attention to the internal structure of the subhalos. The simulations used in this work do not fully resolve density profiles in the innermost $\sim 500$ pc of dwarf halos, but integral properties such as $V_{\text{max}}$ and $R_{\text{max}}$ are converged for $V_{\text{max}} > 15$ km s\textsuperscript{-1} objects. These two quantities fully define the two-parameter Navarro-Frenk-White (NFW; Navarro et al. 1996) density profile

$$\rho(r) = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2},$$

where $r_s = R_{\text{max}}/2.1626$ is a characteristic scale radius and $\rho_s = \rho(r=R_{\text{max}}, V_{\text{max}})$ is four times the density at $r = r_s$. We may therefore extrapolate a unique circular velocity curve into the inner regions of the halos to make predictions regarding the central densities and compare with observations at small radii. This extrapolation assumes that the inner structure of subhalos is not strongly dependent on cosmology (i.e. that subhalos still follow NFW profiles in BICEP2); for WDM\textsubscript{2.6keV} at least, this extrapolation seems to be valid (Dunstan et al. 2011), but we note that varying the density profile can strongly impact the number of massive failures (Di Cintio et al. 2013; Garrison-Kimmel et al. 2014b). Similarly, we may predict the relative change in the annihilation signal from substructure by knowing only the relationship between $V_{\text{max}}$ and $R_{\text{max}}$, as the signal from a single halo or subhalo is proportional to $\rho_s r_{\text{vir}}^3$ (Strigari et al. 2008).

We thus begin our investigation by presenting this relationship for subhalos of the main host (within 300 physical kpc, for comparison to the MW satellites) in the four

$\begin{array}{cccccccc}
\text{MC} & R_{\text{vir}} \ (h^{-1} \text{M}_\odot) & V_{\text{max}} \ (\text{km s}^{-1}) & V_{\text{c}} \ (\text{km s}^{-1}) & N_s (< R_v) & N_p (< R_v) & r_{\text{uncont}} \ (h^{-1} \text{Mpc}) & N_h (< 1 h^{-1} \text{Mpc}) \\
\text{BICEP2} & 1.26 & 221 & 156 & 460 & 8.8 \times 10^6 & 1.27 & 1.32 \\
\text{Planck} & 1.49 & 231 & 166 & 944 & 9.4 \times 10^6 & 1.04 & 2.16 \\
\text{Low-\text{\(\Omega_M\)}} & 1.21 & 222 & 176 & 709 & 9.3 \times 10^6 & 1.05 & 1.66 \\
\text{WDM}\textsubscript{2.6keV} & 1.49 & 231 & 194 & 119 & 9.4 \times 10^6 & 0.97 & 7.6 \\
\end{array}$

Table 2. The properties of the main host halo in the zoom-in simulations. In order, the columns are the virial mass $M_{\text{c}}$, virial radius $R_v$, maximum circular velocity $V_{\text{max}}$, virial velocity $V_{\text{c}} = \sqrt{GM_{\odot}/R_v}$, the number of resolved ($V_{\text{max}} > 8$ km s\textsuperscript{-1}) subhalos within the virial radius $N_s(< R_v)$, the number of simulation particles within the virial radius $N_p$, the distance to the nearest low resolution particle $r_{\text{uncont}}$, and the number of halos with resolved internal structure ($V_{\text{max}} > 15$ km s\textsuperscript{-1}) within $1 h^{-1}$ Mpc, $N_h(< 1 h^{-1} \text{Mpc})$.
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![Figure 6](image.png)

Figure 6. The relationship with $R_{\text{max}}$ and $V_{\text{max}}$ for subhalos in the BICEP2 (black circles), Planck (cyan squares), Low-$\Omega_M$ (magenta triangles), and WDM$_{2.6\text{keV}}$ (yellow diamonds) cosmologies, along with power-law fits to the data (Equation 3). The fits are weighted by $V_{\text{max}}$ with the log-slope held fixed at the best-fit value in the Planck model, $p = 1.419$ (though there are weak indications that the slope is steeper in the BICEP2 model). The best-fit normalization in the BICEP2 cosmology is 35% lower than in the Planck simulation. In addition to helping to alleviate TBTF (see Figure 7), this overall shift in $R_{\text{max}}$ at fixed $V_{\text{max}}$ also implies a ~35% lower annihilation signal from each subhalo in BICEP2. The normalizations, $A$, are 0.71 (Planck), 0.75 (Low-$\Omega_M$), 0.73 (WDM$_{2.6\text{keV}}$), and 1.09 (BICEP2).

### Cosmological Models

Plotted in Figure 6 are the individual $R_{\text{max}} - V_{\text{max}}$ values for subhalos in each model, with the BICEP2 model plotted as black circles, the Planck model in cyan squares, the Low-$\Omega_M$ model as magenta triangles, and the WDM$_{2.6\text{keV}}$ model as yellow diamonds. The lines plot power-law fits to the subhalos:

$$R_{\text{max}} = A \left( \frac{V_{\text{max}}}{10 \text{ km s}^{-1}} \right)^p.$$  

The contribution to the least-squares fit from each halo is weighted by $V_{\text{max}}$ with the log-slope held fixed at the best-fit value in the Planck model, $p = 1.419$, allowing the normalization $A$ to vary. The three Planck-like models agree nearly perfectly: the normalizations differ by only 5%. The BICEP2 model, however, is clearly offset from the remaining three cosmologies with a normalization 35% higher.

It is interesting to note that the WDM$_{2.6\text{keV}}$ model yields similar subhalo structural parameters ($V_{\text{max}} - R_{\text{max}}$) to those of the Planck models, at least for the velocity range plotted here. Below we show that this is not the case for field halos in WDM$_{2.6\text{keV}}$, which are less concentrated than Planck halos in the field. We interpret this difference as an effect of enhanced subhalo stripping for the WDM$_{2.6\text{keV}}$ subhalos. Host halos tend to strip matter from the outer parts of subhalos, making them more concentrated with time. The WDM$_{2.6\text{keV}}$ host halo density and mass remain similar to that in Planck cosmology, and the relative stripping experienced by the low-concentration infalling subhalos is more significant than it is in any of the other models. This is also consistent with the fact that we see fewer subhalos in the WDM$_{2.6\text{keV}}$ case.

The differences seen in Figures 5 and 6 impact the counts of discrepant TBTF halos. We directly compare the circular velocity curves predicted for each of our runs to observations of the classical MW dwarf spheroidal (dSphs) galaxies in Figure 7 – each line represents a single subhalo within 300 kpc and each point indicates a MW satellite. The left panel plots the Planck model, the central panel indicates the results in WDM$_{2.6\text{keV}}$, and the right panel plots subhalos in the adopted BICEP2 cosmology. As in Boylan-Kolchin et al. (2011, 2012), the observational sample is comprised of the galaxies within 300 kpc of the MW with $L > 10^7 L_\odot$, excluding the Magellanic Clouds and the Sagittarius dwarf. The former is removed from the sample because satellites as large as the Clouds are rare around MW-size hosts (Boylan-Kolchin et al., 2010, Busha et al., 2011, Tollerud et al., 2011); we remove the latter because it is currently interacting with the MW disk and is therefore not in equilibrium. For the remaining dwarfs, we plot $V_{1/2}$ at $r_{1/2}$, the circular velocity at the half-light radius, with $1\sigma$ errors in Figure 7. The values are taken from Wolf et al. (2010), who used data from Walker et al. (2009), Muñoz et al. (2005), Koch et al. (2007), Simon & Geha (2007) and Mateo et al. (2008).

The lines in Figure 7 each indicate NFW rotation curves for a single subhalo of the central host. The dashed lines indicate the simulated analogs to the Magellanic Clouds, defined here as subhalos with $V_{\text{max}} > 60$ km s$^{-1}$, which we remove from our analysis and plot only for illustrative purposes. The dotted lines indicate circular velocity profiles that fall below the $1\sigma$ error on $V_{1/2}$ for at least one of the MW dSphs – these subhalos are nominally consistent with the observational data and can host a MW satellite. The solid lines, however, have circular velocities that lie above all the dSphs and therefore qualify as “massive failures” – subhalos without observational counterparts. Nearly all of these massive failures are large enough, even today, to have formed stars in the presence of an ionizing background (Bullock et al., 2000, Somerville, 2002, Sawala et al., 2014).

Though the TBTF problem remains evident in all three models plotted here, the number of massive failures is noticeably reduced in the BICEP2 cosmology relative to the Planck model. Perhaps surprisingly, the running power spectrum of BICEP2 eliminates more massive failures than the chosen WDM free-streaming cutoff. Moreover, the remaining massive failures in the BICEP2 model lie well below the TBTF solution. Below we show that this is not the case for field halos in WDM$_{2.6\text{keV}}$, which are less concentrated than Planck halos in the field. We interpret this difference as an effect of enhanced subhalo stripping for the WDM$_{2.6\text{keV}}$ subhalos. Host halos tend to strip matter from the outer parts of subhalos, making them more concentrated with time. The WDM$_{2.6\text{keV}}$ host halo density and mass remain similar to that in Planck cosmology, and the relative stripping experienced by the low-concentration infalling subhalos is more significant than it is in any of the other models. This is also consistent with the fact that we see fewer subhalos in the WDM$_{2.6\text{keV}}$ case.

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10 We have also tested a quadratic fit in log-space and do not find evidence for a rollover at small $V_{\text{max}}$, though there are weak indications that the slope is steeper for the BICEP2 subhalos.

11 Though we do not plot it, the central halo in the Low-$\Omega_M$ cosmology hosts eight massive failures.

12 Though a lighter WDM mass will be more effective (e.g., Schneider et al., 2013), it is constrained by the Ly-$\alpha$ forest (Viel et al., 2013) and subhalo counting (Polsensky & Ricotti, 2011).
of formation and tidal stripping after infall onto the central host (Bullock et al. 2001; Ludlow et al. 2014). To more directly probe the former, Figure 8 plots $R_{\text{max}}$ and $V_{\text{max}}$ for halos in the field surrounding the central host, along with power-law fits (Equation 3) with $p$ again held fixed at best fit value in the Planck simulation, $p = 1.26$. We limit ourselves to objects at least 500 kpc from the central host to avoid the majority of “backsplash” galaxies that have interacted with the host in the past (Teyssier et al. 2012; Garrison-Kimmel et al. 2014a), which may have undergone significant tidal stripping, and we select halos within 1.5 Mpc to avoid high mass (low resolution) contaminating particles.

While the agreement between the Planck and Low-$\Omega_M$ models remains in the field (as expected due to similar power spectra), the effects of the modifications to $P(k)$ are apparent in both the WDM$_{2\,6keV}$ and BICEP2 simulations. The latter two display significantly lower density halos, consistent with the suppression in power spectra at the time of formation; the fits to both are $\sim 50\%$ higher than the fit in the Planck cosmology. The most massive nearby field halo in the BICEP2 simulation is undergoing a major merger, resulting in an anomalously large $R_{\text{max}}$ and we therefore perform the fit with and without that object. Including it results in the fit plotted as a black dashed line; the fit without that point is plotted as a solid black line.

4 CONCLUSIONS

We have tested the impact of the suppressed small-scale primordial power spectrum suggested by the recent BICEP2 results by simulating structure formation both with the “running” power spectrum suggested by these results and with the cosmology suggested by the Planck experiment, and using two control models – the Planck model with a free-
streaming cut-off corresponding to a WDM particle mass of 2.6 keV (thermal) and the \textit{Planck} power spectrum with an artificially lowered $\Omega_m$. We have simulated the evolution of identical ($50 \, h^{-1} \, \text{Mpc})^3$ volumes from $z = 125$ until $z = 3$ and the formation of a MW-size host until $z = 0$ at high resolution. These simulations indicate that the suppression in the primordial power spectrum at small scales results in mild offsets in the large-scale halo mass function (consistent with expectations from linear theory) and non-trivial differences in the subhalo $V_{\text{max}}$ function and the inner structure of both field and satellite halos. Specifically:

- The $V_{\text{max}}$ function of subhalos around a MW-size host in the \textit{BICEP2} cosmology lies well below that of the same host in the \textit{Planck} model for $V_{\text{max}} \lesssim 40 \, \text{km s}^{-1}$, even after normalizing for the differing sizes of the hosts. There are twice as many resolved ($V_{\text{max}} > 8 \, \text{km s}^{-1}$) subhalos within the virial radius of the central host in the \textit{Planck} simulation as result in the \textit{BICEP2} cosmology. The \textit{Planck} and $\Omega_M$ models agree after scaling for the host mass. Unsurprisingly, the WDM $2.6\,\text{keV}$ simulation results in only $\sim 10\%$ as much substructure as our fiducial \textit{Planck} run.

- Although masses of the largest subhalos around our selected host appear to be mostly unaffected by the changes in cosmology, the average concentrations (quantified here by the relationship between $R_{\text{max}}$ and $V_{\text{max}}$) of subhalos are significantly lower in the \textit{BICEP2} cosmology than any of the \textit{Planck}-like models and our WDM $2.6\,\text{keV}$ run. This increase in $R_{\text{max}}$ at fixed $V_{\text{max}}$ alleviates the too-big-to-fail problem, and may increase the efficacy of baryonic processes that could further reduce the central densities.

- Taken together, the above two results imply that the substructure “boost,” the contribution to the dark matter annihilation signal due to subhalos, is at least a factor of $\sim 5$ times smaller in the \textit{BICEP2} cosmology. Although the absolute value of the boost depends on many assumptions and is an uncertain quantity, this relative modification should be more robust and will work to lower previous upper limits to order unity.

While the above conclusions are drawn from simulations of only a single MW-size host halo, the overall trends demonstrated should hold for all such systems. Though there is significant scatter between MW-size systems (e.g. Boylan-Kolchin et al. 2010), the relative offset from the mean in the substructure population of a single host appears to remain largely static across cosmologies (Horiuchi et al. 2014). Therefore, the precise magnitude of the above changes may vary, but the general result that subhalos are less numerous and less dense in the \textit{BICEP2} model compared to \textit{Planck} is robust. In order to accurately determine the range of substructure suppression and changes in concentration, one requires a large sample of simulations similar to those shown here; we elect to instead illustrate the general trends only.

Our results indicate that the level of spectral index running that reconciles the \textit{BICEP2} measurement with other constraints has interesting effects on dark matter structure over a range of scales. These changes are most evident at the smallest scales, where they help to alleviate small-scale issues with CDM. Though not addressed here, this type of reduction in small-scale power could have interesting implications for understanding cosmic reionization, which may require the early collapse of small halos and thus a fair amount of power on $\sim 10^8 \, M_\odot$ scales (e.g. Somerville et al. 2003 Robertson et al. 2013), and conversely studies of the early Universe may constrain the allowed running (similar to the constraints placed on WDM by Schultz et al. 2014). Signs of a non-trivial primordial power spectrum may also be explored in the Ly-$\alpha$ forest.

While it should be noted that inflationary models with precisely constant running at the level we have investigated have difficulty producing enough $e$-foldings (Easther & Peiris 2006) and likely have higher order corrections to the power spectrum in this parameterization (Abazajian et al. 2005), there are feasible models with scale-dependent running that produce similar suppression of power at dwarf scales to that considered here (e.g. Kobayashi & Takahashi 2011 Wan et al. 2014). The broad point of this work is to highlight the salient role that a non-trivial primordial power spectrum has in affecting small-scale predictions in \textit{LCDM}. In light of the exciting \textit{BICEP2} results interpreted as evidence for inflationary gravitational waves, the need to consider non-standard primordial power spectra in structure formation studies has grown all the more urgent.

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