Using Sequence Ensembles for Seeding Alignments of MinION Sequencing Data

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Abstract

Oxford Nanopore MinION sequencer is currently the smallest sequencing device available. While being able to produce very long reads (reads of up to 100 kbp were reported), it is prone to high sequencing error rates of up to 30%. Since most of these errors are insertions or deletions, it is very difficult to adapt popular seed-based algorithms designed for aligning data sets with much lower error rates.

Base calling of MinION reads is typically done using hidden Markov models. In this paper, we propose to represent each sequencing read by an ensemble of sequences sampled from such a probabilistic model. This approach can improve the sensitivity and false positive rate of seeding an alignment compared to using a single representative base call sequence for each read.

1 Introduction and Background

In this paper, we explore the use of simple \( k \)-mer seeding strategies for mapping MinION reads to the reference sequence. MinION base calls can have up to 30% error rate which poses a significant challenge for read mapping. Instead of a single read sequence as a query, we propose to use an ensemble of sequences sampled from a hidden Markov model used for base calling. With such ensemble of sequences representing alternative predictions of the true read sequence, we were able to design a simple seed that allows for 99.9% sensitivity with a very small number of false positives on real data.

MinION is currently the smallest and most portable sequencing machine available. Besides the small size, the advantage of the technology is its ability to sequence very long reads (reads as long as 100 kbp were reported). To sequence DNA, MinION uses measurements of electric current as a single stranded fragment of DNA passes through a nanopore. The electric current depends mostly on the context of \( k \) bases of DNA passing through the pore at the time of the measurement. As the DNA fragment moves through the pore, this context changes and measurements change accordingly.

The raw measurements are first processed by MinKnow software from Oxford Nanopore. MinKnow uses an on-line algorithm to split raw measurements into events, where each event would ideally correspond to a single-base shift of the DNA through the pore. Each event is characterized by the mean and the variance of the corresponding raw measurements. This sequence of events is then uploaded to a cloud-based service Metrichor for base calling.

Exact details of the algorithms behind MinKnow and Metrichor are not disclosed by Oxford Nanopore. However, the whole process is naturally modelled by a hidden Markov model (HMM) \( \text{Durbin et al. 1998} \) Chapter 3 with hidden states corresponding to \( k \)-mers of underlying DNA sequence, where observations would represent mean values of the current in each event. In fact, data provided by Oxford Nanopore include parameters of such a model. Open-source base caller based on this idea was recently implemented by \( \text{David et al. 2016} \) in Nanocall software, with accuracy similar to Metrichor. To decode the sequence of observations, Nanocall uses the standard Viterbi algorithm \( \text{Viterbi 1967} \) for finding the most probable
state path. Another open-source base caller DeepNano uses instead recurrent neural networks (Boža et al., 2016).

Base calls produced by the Viterbi algorithm contain many errors (David et al., 2016; Boža et al., 2016); a typical error rate would be around 30%, dominated mostly by insertions and deletions. With these characteristics, even basic tasks, such as mapping the reads to the corresponding reference sequence, become a challenge.

Currently, two general-purpose aligners are used in the community to map MinION reads: BWA-MEM (Li and Durbin, 2010), and LAST (Kiebasa et al., 2011). Both of these tools follow a general seed-and-extend paradigm, well-known from BLAST (Altschul et al., 1990). First, they build an index of one of the sequences (e.g., the reference genome), in which they can quickly locate exact matches of seeds that originated from the query sequence (the read). In this way, they identify regions in the reference sequence (called hits of a seed) that are likely to contain an alignment. In these regions, they perform an extension phase, which will identify the target alignment. The sensitivity of such tools depends largely on how likely is a real alignment to contain a hit of a seed (without the hit, the extension phase is not triggered, and the alignment is not identified). On the other hand, the running time depends on how many false hits will trigger unnecessary extensions.

The original BLAST (Altschul et al., 1990) used 11 consecutive matches as a seed. Consecutive matches of a fixed length are very easy to index by standard hashing techniques. For mapping of sequences with a small number of errors to corresponding reference sequences, longer seeds were used, offering more specificity (e.g., BLAT (Kent, 2002)). BWA-MEM and LAST use variable seed lengths, indexed with FM-index (Ferragina and Manzini, 2000) or suffix arrays (Manber and Myers, 1993); by extending seeds to the point of only a few occurrences, one can avoid most costly false positives. The adjustments for MinION reads in case of BWA-MEM and LAST include lowering the minimum length of a seed to be considered as a valid hit, and changes that make the extension phase less stringent. GraphMap tool (Sovic et al., 2016), specifically targeting MinION data, has been recently released. GraphMap uses seeds allowing insertions and deletions in the context of a complex multi-step algorithm that goes well beyond a simple seed-and-extend framework.

All of these tools consider Metrichor base calls, equivalent to the most probable state path in the HMM, as the query sequence. Our goal in this paper was to explore sub-optimal decodings of the HMM and attempt to solve the challenges imposed by MinION reads by using an ensemble of sub-optimal sequences instead of a single DNA sequence. To this end, we have implemented a sampling algorithm (see, e.g. Cawley and Pachter (2003)) that can generate samples from the posterior distribution of state paths given the sequence of observations. We adapt common seeding strategies to such ensembles of sequences and show that on real data we can find a seed that is easy to index, 99.9% sensitive, and yields only a small number of false positives that would trigger extension phase unnecessarily.

Sampling of MinION base calls was also considered by Szalay and Golovchenko (2015). They use sampling from the base calling HMM to arrive at the correct consensus sequence for an alignment of multiple reads. Due to the nature of errors in MinION reads and availability of a reasonable probabilistic model, we consider sampling strategies to be a promising alternative in many applications of MinION.

2 HMM for Sampling MinION Base Calls

Both Oxford Nanopore Metrichor base caller and recently released open-source base caller Nanocall (David et al., 2016) use hidden Markov models. Briefly, each hidden state of the HMM represents one k-mer passing through the pore, and the emission of the state is the value of the electric current. Actual measurements of current provided by the device with high sampling rate are segmented by the MinKnow software into discrete events, each corresponding to the shift of the DNA sequence through the pore by a single base. The base callers then use an HMM to obtain the sequence of hidden states given the sequence of events from the MinION read.

Definition of the model. Our HMM follows the same general idea. The set of states of our HMM is composed of all k-mers (we denote state for a k-mer x by $S_x$) and the starting state $S_0$. Different versions
of MinION use different values of \( k \); in our experiments we have used a data set with \( k = 5 \), while the newer chemistry uses \( k = 6 \).

Emission of state \( S_x \) is represented as a continuous random variable. The probability of observing a measurement \( e \) for a \( k \)-mer \( x \) is given as

\[
Pr(e | x) \sim \mathcal{N}(\text{scale} \cdot \mu_x + \text{shift}, \sigma_x \cdot \text{var}),
\]

where \( \mathcal{N}(\mu, \sigma) \) is a normal distribution with mean \( \mu \) and standard deviation \( \sigma \). Parameters \( \mu_x, \sigma_x \) (specific for each version of the chemistry and each \( k \)-mer \( x \)), and \( \text{scale}, \text{shift}, \text{var} \) (scaling parameters specific for each read) are provided by Oxford Nanopore and can be obtained from the FAST5 file containing each read. Starting state \( S_0 \) is silent.

Under ideal conditions, each event corresponds to a shift by a single base in the DNA sequence. This corresponds to four outgoing transitions from each state \( S_x \) to state \( S_y \), where \( x \) and \( y \) overlap by exactly \( k-1 \) bases (i.e., \( S_{AACTG} \) has transitions to states \( S_{ACTGA}, S_{ACTGC}, S_{ACTGG}, \) and \( S_{ACTGT} \)). This organization closely resembles de Bruijn graphs commonly used in sequence assembly (Pevzner et al., 2001). All four transitions have an equal probability. From the starting state \( S_0 \), we have a transition to each possible \( S_x \) with equal probability \( 1/4^k \).

Segmentation of raw measurements into events is known to be error prone. In particular, two events with similar measurements can be fused together, or a single event can be split artificially into multiple events. Thus the assumption that each event corresponds to a single-nucleotide shift is unrealistic. To account for this fact, we have introduced additional transitions in our model.

First, we have added a self-transition (so-called split transition) to each state, which models splitting of a single true event into multiple predicted events. Second, we have also added so-called skip transitions between all pairs of states \( S_x \) and \( S_y \), which would correspond to shifts of the \( k \)-mer by up to \( k \) bases instead of one.

The transitions probabilities for split and skip transitions are not provided by MinION. We have estimated these parameters directly from the data, as outlined in Section 3. Alternately, we could employ a more elaborate error model for Oxford Nanopore event segmentation process.

**Inference in the model.** A traditional way of decoding HMMs is by finding the most probable sequence of states by the Viterbi algorithm (Viterbi, 1967), which is the approach taken both by Metrichor and Nanocall. The resulting sequence of states (which is, in fact, a sequence of \( k \)-mers corresponding to individual events) can be translated into the DNA sequence. In most cases, the neighbouring \( k \)-mers in the sequence should be shifted by one, and thus each state in the sequence should introduce one additional base of the DNA sequence. However, split and skip transitions may introduce between 0 and \( k \) bases for each event. In these cases, the result is not necessarily unique: for example state sequence \( S_{ACTCTC}S_{CTCTCA} \) could correspond to one of the sequences ACTCTCA, ACTCTCTCA, ACTCTCTCTCA, or even ACTCTCTCTCTCA. We have decided to adopt the shortest possible interpretation, as is done in Nanocall.

Since the base calls produced by the Viterbi algorithm contain many errors, we have decided to explore the use of an ensemble of alternative sequences instead of a single base call sequence. To this end, we have implemented the stochastic traceback algorithm (see, e.g., Cawley and Pachter (2003)) to generate samples from the posterior distribution of state paths given the sequence of observations.

Briefly, for a given sequence of observations \( e_1, e_2 \ldots e_n \), the algorithm starts by computing forward probabilities, where probability \( F(i, s) \) is the probability of generating first \( i \) observations \( e_1, e_2 \ldots e_i \), and ending in state \( s \) (Rabiner, 1989). The last state \( s_n \) of the path is sampled proportionally to the probabilities \( F(n, s_n) \). When state \( s_n \) is fixed, we can sample state \( s_{n-1} \) proportionally to \( F(n-1, s_{n-1}) \cdot t_{s_{n-1}, s_n} \), where \( t_{s,s'} \) is the transition probability from state \( s \) to state \( s' \). This can be continued, until we sample the complete path \( s_1 \ldots s_n \). The running time of the algorithm is \( O(nm^2) \), where \( n \) is the length of the sequence and \( m \) is the number of states. Forward probabilities need to be computed only once if multiple samples are required for the same read.

Figure 1 illustrates typical differences between individual samples. Note that the samples are almost identical in some regions, but these conserved regions are interspersed by regions with very high uncertainty.
Figure 1: Example of base calling samples from a MinION read. The first line corresponds to the Viterbi base call, other lines correspond to four samples from the posterior distribution defined by the HMM. Base calls were aligned according to events in the sequence of observations.

This is a typical pattern for MinION data.

3 Experiments

Data preprocessing and model training. For our experiments, we have used a data set from *E. coli* (strain MG1655) with accession number ERR968968 produced by the Cold Spring Harbor Laboratory by using MinION sequencer with SQK-MAP005 kit. For simplicity, we have only considered template reads (complement reads from the reverse strand use different model parameters).

To filter out low quality reads, we have mapped Metrichor base calls to the reference sequence by BWA-MEM ([Li and Durbin](2010)) with `-x ont2d` parameters optimized for mapping Oxford Nanopore reads. The reads that did not map to the reference at all were discarded. We also discarded reads where Metrichor predicted skips in the event sequence longer than two. From the original 27,073 reads, we were left with 25,162 reads.

From these reads, we have randomly selected a training set (693 reads) and a testing set (307 reads). The training set was used to estimate the transition probabilities in our HMM. In particular, we set the probability of each transition to be proportional to the number of times the transition was observed in the training data set. We added pseudocount of 1 to avoid zero transition probabilities for rare transitions.

Preparing testing data. For each sequence in the testing set, we have produced a Viterbi base call and 250 samples from the posterior distribution as outlined in Section 2. Figure 2 shows comparison of sequence identities of individual base calls to the reference genome. Note that our Viterbi base calls are not too different from Metrichor base calls; slight decrease in the quality of calls is expected due to simplicity of the model we have used (the decrease in the sequence identity is similar to that observed by [David et al.](2016)). Sampled sequences have in general lower sequence identity than the Viterbi base call, as can be expected, since they are mostly sub-optimal paths through the model. However, the difference from the Viterbi base call identities is not very high.

Experimental setup and evaluation. Our goal is to consider various seeding strategies for seed-and-extend algorithms similar to BLAST ([Altschul et al.](1990)). Briefly, a typical seed-and-extend algorithm first uses an index structure to locate hits between the query sequence and the target. For example, the most basic BLAST strategy looks for exact matches of length 11. Second, we try to extend each cluster of hits to a full alignment. The extension phase usually involves dynamic programming and is therefore time consuming.

The seed-and-extend algorithms cannot locate alignments that do not contain a hit of the seed between the query and the target sequence. We call these alignments *false negatives*. Note that even a single hit is
Figure 2: Comparison of sequence identity to the reference genome for Metrichor base calls, our Viterbi base calls, and posterior samples for 40 randomly selected reads. All sequences were aligned to the reference by BWA-MEM. Sequence identity of Metrichor, Viterbi, and a box plot distribution of sequence identities of 250 samples are shown on the y-axis.

often sufficient to locate the whole alignment, depending on the particular extension strategy. On the other hand, there will be spurious hits between random locations which will trigger extension. These spurious hits often dominate the running time of the alignment algorithm, and consequently, we need to minimize their number. We call such spurious hits false positives.

To evaluate application of various seeding strategies in MinION data, we will split our data set into windows, each corresponding to 500 events. More precisely, for each read all base calls and samples were aligned to each other based on event boundaries: we have padded all sequences generated for one event in individual samples by gap symbols so that they have the same length (see also Figure 1). The resulting multiple alignment was then split into windows which will represent our query sequences.

The Viterbi base call sequence from each window was aligned to the reference genome by LAST software (Kielbasa et al., 2011) with parameters -q 1 -a 1 -b 1 -T 1. We have kept only those windows that aligned to a unique place in the genome, and the alignment covered the entire length of the window. After this step, we were left with 3192 windows out of 4948. A randomly chosen subset of 143 windows was used as a validation set for exploring various seeding strategies, and the remaining 3049 windows were used for final testing. The region of the reference covered by the alignment to the window is considered to be the
only true alignment of the window to the reference sequence.

When testing an alignment seeding strategy, we try to locate a particular seed in both the query window and the reference sequence. We represent the hit of the seed by the coordinates of the left endpoints of the hit in the query window and in the reference. The seed hit is considered to be valid, if the endpoint in the reference is within the region covered by the alignment of this particular window and on the correct strand. The entire window of a read is considered to be a true positive (TP), if it contains at least one valid hit; we assume that the extension algorithm would be able to recover the alignment within this window starting from this seed. The sensitivity (Sn) of the seeding strategy is the number of true positives divided by the total number of windows.

Many seed hits are invalid, and they contribute to the false positive rate. Often we see clusters of seeds with very similar coordinates in both reference and the query window. Presumably the extension algorithm would be called only once for each such cluster. Therefore, we compute the number of false positives by greedily selecting one seed from each cluster so that each seed differs in both coordinates by at most 10 from a selected read.

**Simple seeding strategies.** The most simple seeding strategy is to consider $k$ consecutive exact matches as a hit. The traditional approach would create an index of all $k$-mers in the reference genome and then scan all $k$-mers in the query windows. Each cluster of matching $k$-mers would trigger the extension phase.

For example, if we consider the Viterbi base calls and use 13 exact consecutive matches as a seed, we will be able to map 98.8% windows to the correct region of the reference (see Fig. 3), but we will also incur a substantial number of false positives (more than 240,000 or about 80 per each query window).

Our strategy of using sampling instead of Viterbi base calls works as follows. In the basic version of our approach (see $t = 1$ in Fig. 3), we consider $k$-mers from $n$ different samples from the HMM for each position in the read window. Each $k$-mer can potentially form the seed triggering the extension phase of the alignment. To match the sensitivity of the Viterbi base calls for $k = 13$, we need only $n = 3$ samples. One advantage of our approach is that we can increase sensitivity by increasing the number of samples $n$. For example with 8 samples we reach 99.9% sensitivity and with 14 samples 100% sensitivity. The cost for this very high sensitivity is a high false positive rate; even with 3 samples we have about 2.6× more false positives than the Viterbi.

To improve the false positive rate, we use a simple prefiltering step: at each position in the window we consider only those $k$-mers that appear in at least $t$ different samples. Assuming that the true sequence has a high posterior probability in the model, we expect that it will occur in many samples, whereas most other variants would occur rarely and thus be filtered out. Indeed, for $t = 4$ we can reach the sensitivity of the Viterbi algorithm with about 20% reduction in the false positive rate, using $n = 25$ samples.

**Multiple seed hits to trigger extension.** We have also considered a more complex seeding strategy, where we first find matching 10-mers and then we join them into chains of length 3. This technique has previously proved to be very effective for regular alignment tasks (Altschul et al., 1997).

Matching 10-mers in the chain are required to have increasing coordinates in both the read and the reference sequence, and the distance between starts of adjacent seeds in the chain must be at least 10 and at most 50 in both sequences. However, the distances of the two 10-mer matches in the two sequences may differ, accommodating indels in the intervening regions. The entire chain is then again represented by its leftmost point in both the read and the reference for the purpose of determining if it is valid.

As we see in Figure 4, this seeding strategy is too stringent for the Viterbi base calls, achieving only 71.3% sensitivity. On the other hand, false positives are extremely rare, totaling only 136 in all 3049 windows.

When using samples, different 10-mer matches in the chain may come from different samples. The chaining of weaker seeds helps to accommodate regions with high uncertainty and many indels present in the MinION data. Some settings of our strategy can achieve the same sensitivity as the Viterbi algorithm with even lower false positives, but more importantly, by considering more samples, we can increase sensitivity while keeping the false positives quite low. For example, for $t = 2$ and $n = 43$ our strategy can reach 99.9% sensitivity with only 6407 false positives.
Figure 3: **Performance of our approach compared to the Viterbi base calls for seeding with a single 13-mer.** The $x$-axis of the plot is the total number of false positives on the whole testing set; the $y$-axis is the number of true positives out of 3049 windows in total. Performance of the Viterbi base calls is shown by the black $X$. Three lines show our approach for different values of threshold $t$ for filtering $k$-mers. Each point on the line represents performance for a particular number of samples $n = 1, 2, \ldots$. The table shows sensitivity and the number of false positives for selected values of $n$ and $t$. In particular for each $t$, we show the smallest value of $n$ achieving sensitivity at least 95%, the sensitivity of the Viterbi algorithm, and sensitivity at least 99.9%.

### 4 Conclusions and Future Work

In this paper, we have examined the problem of mapping MinION sequencing reads to the reference sequence. The error rate of MinION reads is very high (approx. 30%), with many insertions and deletions. Consequently the standard sequence alignment techniques do not achieve sufficient sensitivity for mapping reads.

Instead of representing the read by a single base called sequence, we have proposed to use an ensemble of sequences generated from the posterior distribution defined by the HMM capturing the properties of MinION sequencing process. We have adapted the standard $k$-mer based techniques for alignment seeding to ensembles of sequences and identified a seed (three 10-mer hits spaced by at most 50 bases) that in our experiments achieved 99.9% sensitivity with an extremely small number of false positives. With such a low false positive rate, we could investigate more precise (and slower) algorithms for the extension phase, which will be the next important step towards sensitive alignment of MinION reads.

An obvious extension of our approach would be to consider spaced seeds \cite{Ma2002}. Our experiments suggest that a typical MinION read consists of short regions of high-confidence sequence (often under 15bp) interspersed with regions of high uncertainty with many indels. The spaced seeds would have to target mainly these high-confidence regions, however, these regions seem to be too short to admit complex seeds of any significant weight. One possibility would be to build a probabilistic model capturing high-confidence and high-uncertainty regions and transitions between them, and attempt to design an optimized spaced seeds, for example by techniques suggested by \cite{Brejova2004}.
Another option would be to use seeds that also allow indels at do not care positions. These types of seeds were successfully used by Sovic et al. (2016) for MinION read mapping, but the overall algorithm was much more complicated than a simple seed-and-extend. Moreover, these types of seeds are much more difficult to index than continuous or spaced seeds and we believe, that our sampling approach together with multiple chained seed hits provides an elegant answer to the problem.

In this work, we have only considered 1D reads from MinION. However, MinION attempts to read both strands of the DNA and then combine the readouts in postprocessing to a single sequence (these are called 2D reads). Since 2D reads are much more accurate (typical error rate is about 15%), most of the researchers using MinION suggest throwing out 1D reads and only use 2D reads in further analysis.

This has two problems. First, usually there is about $4 - 5 \times$ more 1D reads than 2D reads that pass Metrichor base calling procedure (Ip et al., 2015). Thus we are throwing out most of the data. Second, recently people have started to use MinION in applications such as monitoring disease outbreaks (Quick et al., 2016). In these applications, reads are analyzed on-the-fly as they are produced, and we cannot rely on postprocessing of base calls.

In future work, we would like to investigate the seed-and-extend approaches to read-to-read alignment. With our sampling approach, we would not need to commit to a single interpretation of either of the sequences, potentially increasing the sensitivity of detecting overlaps between reads in a given data set. Sensitive read-to-read alignment is essential for de novo assembly.

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