Search for sub-GeV Dark Matter via Migdal effect with an EDELWEISS germanium detector with NbSi TES sensors

The EDELWEISS collaboration reports on the search for Dark Matter (DM) particle interactions via Migdal effect with masses between 32 MeV·c⁻² to 2 GeV·c⁻² using a 200 g cryogenic Ge detector sensitive to simultaneously heat and ionization signals and operated underground at the Laboratoire Souterrain de Modane in France. The phonon signal was read out using a Transition Edge Sensor made of a NbSi thin film. The detector was biased at 66 V in order to benefit from the Neganov-Trofimov-Luke amplification and resulting in a resolution on the energy of electron recoils of 4.46 eV_{ee} (102.58 eV at 66 V) (RMS) and an analysis threshold of 30 eV_{ee}. The sensitivity is limited by a dominant background not associated to charge creation in the detector. The search constrains a new region of parameter space for cross-sections down to 10⁻²⁹ cm² and masses between 32 and 100 MeV·c⁻². The achieved low threshold with the NbSi sensor shows the relevance of its use for out-of-equilibrium phonon sensitive devices for low-mass DM searches.

I. INTRODUCTION

The direct search for Dark Matter (DM) particle interactions with nuclei in a terrestrial target has made huge progress for particles with masses in the range from 1 GeV·c⁻² to 1 TeV·c⁻². The absence of signal in that region has intensified the interest for the extension of the search to masses down to 1 GeV·c⁻² and below. However, these lower masses raise additional experimental challenges: the need to lower the energy detection threshold well below 1 keV, the ionization or scintillation yield for nuclear recoil signals, and the appearance of new types of backgrounds at the lowest energies. New detector designs targeting low energy threshold include cryogenic detectors [14, 16], CCDs [17, 18] and low-threshold point-contact germanium ionization detectors [19]. DM particles with masses below 1 GeV·c⁻² and with large nucleon-elastic scattering cross-sections are yet to be excluded by direct searches, prompting some searches to be performed above ground [20, 21].

In parallel, it was noticed that the problem of the very low kinetic energy of the nuclear recoil, combined with the reduced ionization or scintillation yield for this type of event, could be circumvented by using the Migdal effect [24, 27]. This effect accounts for the probability that the collision between the DM particle and the nucleus may be accompanied by the release of an atomic electron. The energy imparted to the latter particle is typically much larger than the kinetic energy of the nuclear recoil [27], and thus easier to detect. In addition,
the ionization yield of the electron is not affected by quenching, resulting in important improvements in the sensitivity of ionization-based searches for DM particles with masses below 200 MeV·c\(^{-2}\)\cite{19, 28, 30}. Although the Midgal effect has never been directly observed in a nuclear collision, and precise calculations require special care for electrons in the outermost electronic shells in solids\cite{31, 32}, upper limits on DM-nucleus collision rates can be extracted from the calculation involving electrons below the valence shell.

Based on the Midgal effect, the EDELWEISS collaboration was able to extend the mass range for the search of DM particles down to 45 MeV·c\(^{-2}\), using a 33.4 g cryogenic Ge detector equipped with a Ge Neutron Transmutation Doped (Ge-NTD) thermal sensor\cite{22}. That range was limited by the energy threshold of 60 eV. The excluded cross-sections were constrained by the background, originating from the poorly shielded, above-ground environment of the detector, but also by a large population of events. Later studies\cite{14} suggested that this population is not associated with the creation of electron-hole pairs, and has been so-called Heat-Only (HO) events. In this paper, we present the results of DM searches using Midgal effect performed in a low-radioactivity underground environment with a cryogenic detector equipped with a NbSi Transition Edge Sensor (TES), developed to reduce the sensitivity of EDELWEISS detectors to HO events, and with a low energy threshold for electron recoil.

The paper is organized as follows. In Sec. II, we present the detector and experimental setup. In Sec. III, we give details of the DM search, including data processing, detector calibration and data analysis. In Sec. IV, we present the extracted limits on DM particles using the Migdal effect. Finally, we conclude in Sec. V.

## II. EXPERIMENTAL SETUP

The DM search was performed at the Laboratoire Souterrain de Modane (LSM, France) using the ultra-low background environment of the EDELWEISS-III cryostat\cite{33}. The detectors are thus protected by a 4800 m.w.e. rock overburden, an outer polyethylene shield of 50 cm, followed by a 20 cm lead shield with an inner layer of 2 cm of roman lead and an inner polyethylene shield with an average thickness of 10 cm.

In an attempt to better understand and consequently control the important background of HO events that affects previous EDELWEISS detectors equipped with Ge-NTD thermistors, a new type of sensor of different design and concept was used in the present search. Beyond material differences between the two sensors, they differ in their sensitivity to thermal and out-of-equilibrium phonons, and could reveal differences in the mechanisms in the formation of the HO and normal signals. The detector used for the search named NbSi209 is a 200 g Ge cylindrical crystal (48 mm in diameter and 20 mm in height) on top of which was lithographed a Nb\(_2\)Si\(_{1-x}\) thin film TES\cite{34}. The 100 nm-thick film is shaped as a spiral with a track width of 160 µm. Fig. I shows the top side of the detector. The film is maintained near the temperature of 44 mK, at which its transition between the superconducting and normal state occurs, with the help of a heater resistance hanged to the copper holder and linked to the detector through gold wire. In its normal state, the film resistance is 2 MΩ. The spiral is split in two equal-resistance halves, resulting in a central phonon sensor with a diameter of 14 mm and an annular ring sensor of 3 mm in width (see Fig. I left), those two halves are read as independent channel. The voltage injected across each TES half is continuously read out using the standard EDELWEISS-III cold-FET based electronics at 100 K\cite{33}. The TES are read with a square current with an intensity of the order of 1 nA modulated at 500 Hz. This current induced a small bias of the order of 0.1 mV. In contrast with the Ge-NTD sensor used in previous EDELWEISS detectors\cite{14, 22, 33}, the TES technology has been shown to be sensitive to out-of-equilibrium phonons\cite{34}. The signal has a rise time of less than 1 ms, and two decay constants of 10 and 100 ms, associated to the electron-phonon time constant in the film and the thermal leak of the detector, respectively.

![FIG. 1. Left: Top side of the NbSi209 200 g detector equipped with a NbSi TES, inside its copper holder. The red circle indicates the position of the 20 mm diameter NbSi sensor. The outer diameter of the crystal is covered with the Al mesh electrode. Right: sketch of NbSi209 detector with the outer and inner halves of equal resistance of the NbSi sensor in red and orange respectively, the Ge crystal in light gray and the Al electrode in dark gray.](image-url)
phonons inside the Ge absorber, the electrodes covering the two flat surfaces are 20 nm thick Al grids with a 4% coverage fraction (10 µm lines with a 500 nm pitch). The top electrode covers the outer annulus beyond the NbSi film, and it is held at a bias of 0 V. The bottom side is fully covered by an electrode biased at a voltage varying between ±66 V. The electrodes are read out separately. The charge collected on the NbSi film is not read out. In addition to collecting charge, the bias applied to the electrodes is such that the drift of N electron-hole pairs across a voltage difference \( \Delta V \) produces additional phonons. Those phonon energies \( E_{NTL} = Ne\Delta V \) (\( e \) is the elementary charge) add to the initial recoil energy. This is the so-called Neganov-Trofimov-Luke (NTL) effect\([35, 36]\). It essentially turns a cryogenic calorimeter (operated at \( \Delta V = 0 \) V) into a charge amplifier with a mean gain \( \langle g \rangle = (1 + e\Delta V/\epsilon_{\gamma}) \), where \( \epsilon_{\gamma} = 3.0 \) eV is the average ionization energy in Ge for electron recoils\([37]\).

The data acquisition system and readout electronics are the same as in \([33]\). The data from the phonon and ionization channels were digitized at a frequency of 100 kHz, filtered, and continuously stored on disk with a digitization rate of 500 Hz. Data were collected between December 2018 and July 2020, during the same cool-down as in \([14]\). The beginning of that time period was devoted to optimize the film working temperature that results in the maximum signal-to-noise ratio when the two TES signals are combined linearly. These conditions are found optimal at a temperature of 44 mK, for inner and outer TES resistance values of 100 and 500 kΩ, respectively. The corresponding resolutions for each sensor are approximately 130 eV, resulting in a combined resolution between 90 and 100 eV, and combination factors close to 50%. These values do not vary significantly with the bias value, within the ±66 V range fixed by the electronics\([33]\). For the NTL gain of \( \langle g \rangle = 23 \) obtained for electronic recoil with a bias of 66 V, this corresponds to a resolution of approximately 4 eV electron-equivalent (eV\(_{ee}\)). The accumulation of trapped charges in the detector is controlled by applying the same method as in Ref. \([14]\).

In April 2019, the detector was uniformly activated using a strong AmBe neutron source. The produced short-lived \(^{71}\)Ge isotope decays by electron capture in the K, L, and M shells, with de-excitation x-ray lines at 10.37, 1.30, and 0.16 keV, respectively. The low energy x-ray lines are locally absorbed, thus providing very good probes of the detector response to a DM signal uniformly distributed inside the detector volume. These are clearly visible in Fig. 2, which shows the energy spectrum for the phonon signal from calibration data recorded at a bias of 66 V.

On that figure, the solid black histogram represents events where the charges collected on both electrodes are equal within the ionization measurement precision \( \sigma = 200 \) eV\(_{ee}\), and the dashed red one, those where the two charge collections differ. This corresponds to two populations. The first population are events occurring in the sub-cylinder volume facing the area delimited by the imprint of the NbSi film, easily tagged by the fact that the bottom electrode collects the entirety of the downward moving charges but the upward-moving ones end their drift in the NbSi film and not including a signal on the top electrode. The second one consists of events where a significant fraction of the charges end up on the cylindrical edge of the detector, and the trapped ones produce an asymmetric signal on the two electrodes. With these tags based on the ionization signals, we observe that the first population corresponds to the tail at the right of the 10.37 keV peak in Fig. 2, while the second one corresponds to the tail in between the two peaks. The same pattern is also observed for the 1.3 keV\(_{ee}\) peak. The black Gaussian peak at 10.37 keV\(_{ee}\) thus corresponds to events occurring inside the volume defined by field lines leading to the top electrode and sufficiently far away from the outer edge of the detector, representing 63% of all K-shell events.

Between 30 and 200 eV\(_{ee}\), the energy range relevant for the Migdal DM search, the ionization criterion (same charge collection on both electrode) cannot reliably separate these populations. Therefore, the criterion will not be applied. In Sec. 11, the efficiency associated with events in the 10.37-keV peak will be kept as a conservative lower limit on the total efficiency of the detector.
III. DARK MATTER SEARCH

The DM search has been performed using the data set recorded when the detector was operated at 66 V and selecting only time periods when the phonon baseline resolution is less than 140 eV RMS. This dataset was recorded from March 2019 to June 2020. The average baseline heat energy resolution in the search sample is 102 ± 12 eV RMS, corresponding to 4.46 ± 0.54 eV_{ee} RMS once the NTL gain (g) is considered. For the ionization channel, the resolution is 210.3 ± 16.3 eV RMS, and stable over time.

The $^{71}$Ge peaks have been used for the calibration of the heat and ionization samples in the four months following the AmBe activation. The ionization calibration was observed to be constant over that period. Calibrations with the 356 keV gamma-ray of a $^{133}$Ba source at the beginning, middle and end of the 19-month data-taking period confirmed this stability. The gain of the heat signal was observed to vary slowly by ±10% depending on cryogenic conditions. This was corrected with a precision better than 1% by monitoring the ratio of the heat and ionization signals of events between 5 and 60 keV, and with a precision of 0.1% in samples where the $^{71}$Ge peaks are observed. The non-linearity of the heat channel was measured using the position of the $^{74}$Ge KLM activation peaks observed at different NTL amplification. It is 5% between 1 and 500 keV, and the precision of the correction at low energy is better than 2%.

In order to set the analysis selection criteria, one out of every two hours of data were blinded and the other half kept to set the analysis selection criteria and excluded from the search. In order to derive conservative constraints on DM interaction, it was decided not to subtract possible backgrounds. This represents 27.9 days of blinded data and 28.8 days of non-blinded data for the reference sample.

The offline trigger is based on an optimal matching filter approach, which is essentially the same procedure as described in [22]. The numerical procedure used is detailed in [35]. The pulses are searched iteratively in the filtered data stream using a decreasing energy ordering criterion. This will induce an energy dependency in the triggering efficiency, especially for low energy events for which the dead time is larger than for high amplitude pulses. In this algorithm, a time window of $\Delta t = 2.048 \text{s}$ is used in the pulse with the largest amplitude. This time window is then excluded from the process at the next iteration, it continues until there is no time interval larger than $\Delta t$ in the data stream. In order to assess the amplitude of the pulses, they are fitted in the frequency domain by minimizing a $\chi^2$ function, based on the standard pulse shape derived from K-peak events.

The dedicated data-driven method used to carefully model this effect and estimate the efficiency energy dependency of the analysis is described in detail in [22] and summarized below. Pulses of known energy randomly selected among the events from the K-line decay are scaled to relevant energies and injected in the data stream at random times. This bank of events contains 10667 traces of K-shell events with energies between 2 and 12.6 keV_{ee}; recorded at 66 V after the activation of the detector. This bank contains all types of events occurring in the detector, including events with incomplete charge collection and events with extra energy from out-of-equilibrium phonons.

Those real pulses are first scaled down to a fraction of 10.37 keV_{ee}, in order to estimate efficiency at the desired energy, and injected at a rate of 0.02 Hz to minimize the induced dead time below 1% of the total trigger dead time rate. The ionization pulses are scaled by the same factor and included in the procedure to take into account the biases induced by the pulse fitting procedure, which yield to a systematic shift of the ionization resolution from 210 to 225 eV.

Fig. 3 shows the efficiency as a function of the scaled and injected pulse energies at various stages of the trig-
triggering and data selection procedure. The first criterion (black line) corresponds to the DAQ electronic resets that induce a dead time of $\sim 2.8\%$. Since the goal is to provide upper limits on event rates, it was decided to only take into account the contribution to the total efficiency of the $65\%$ of event present in the K-peak (events with energies $\leq [9.6, 11]$ keV), the associated $35\%$ drop in efficiency across all the energy range is shown by the purple line. This gives a lower limit on the efficiency that can underestimate the signal up to $50\%$ as it effectively treats part of the potential signal as any other background, but it has the advantage of not depending on the detailed understanding and modeling of the tails of the K-peak due to incomplete charge collection and additional energy from out-of-equilibrium phonons. The efficiency of the trigger procedure as a function of the injected energy is described by the blue line. The slightly rising curve slope between $0.8$ and $10$ keV in Fig. 3 is due to the bias of the trigger algorithm favoring high energy events, increasing the dead time for low energy events. The much steeper curve slope between $0.02$ and $0.8$ keV reflects the large number of events coming from electronic noise. The orange and red lines in Fig. 3 correspond to the criterion applied on the pulse shape of the ionization and heat signals respectively, through the fitted $\chi^2$ which help to reduce contamination from pileup and badly reconstructed events. With these criteria, the plateau efficiency is obtained at $1$ keV ($30$ eV$_{ee}$). This threshold is considerably better than the one achievable with the ionization channel alone. However, the following analysis considers different criteria on the ionization energy whose impact is shown in Fig. 3.

As can be seen in Fig. 2, there is a rise in the event rate below $200$ eV$_{ee}$ ($4.6$ keV). As will be shown in the discussion (see Sec. V), these events are not associated with the production of electron-hole pairs in the detector, and are hence so-called as Heat-Only events. Those events are pure heat as no ionization is associated with their heat energy deposit. This population can be reduced by requiring the presence of a significant ionization signal. However, the performance of such criterion at low energy is limited by the ionization resolution of $210$ eV. The green lines in Fig. 3 show the effect of requiring a minimal ionization signal of $100$, $200$, $300$ or $400$ eV on the efficiency. The efficiency loss corresponds to what is expected by the observed Gaussian noise of ionization signals. The optimization of this criterion will be discussed in Sec. IV.

The efficiency-corrected spectrum of the blinded dataset is shown in Fig. 4. The efficiency curve applied is the one corresponding to the criterion requiring more than $400$ eV of ionization energy (darkest green curve in Fig. 3). This efficiency curve will be the one applied to the signal in Sec IV. At high energy, the spectrum is dominated by the $1.3$ keV$_{ee}$ L-peak shifted up to $29.9$ keV after the NTL boost.

![Efficiency-corrected energy spectrum of the blinded part of the dataset after nominal analysis data selection and $E_{\text{ion}} > 400$ eV criterion (corresponding to the efficiency curve in dark green in Fig 3).](image)

**IV. RESULTS**

The data shown in Fig. 3 have been interpreted in terms of limits on the spin-independent interaction of DM particles with target atoms through the so-called Migdal effect. This effect states that an interaction of a DM particle with an atom may induce simultaneously a nuclear recoil and the ionization of an electron. Calculations for non-isolated atoms in semiconductors have been performed [39–41]. They show that the Migdal effect at low energy is enhanced in semiconductor with respect to isolated atom. These calculations are still evolving. However, in Ge, the contribution to this effect comes from $n = 4$ valence shell electrons and mostly yields signals below $30$ eV. Consequently, as done in [22], we use instead the widely used calculations from [27, 31]. Those isolated-atom calculations do not take into account the full band structure of Ge in a crystal, and therefore only the contribution of the $n = 3$ shell is considered, in order to yield conservative rate limits. As this shell gives no signal below $30$ eV$_{ee}$, an analysis threshold is set at this energy, corresponding to a phonon energy of $690$ eV. The contribution from $n \leq 2$ shells has also been neglected, since it does not yield an exploitable signal in our detector because of the very
low probability of emitting an electron from this shell.

As in [22], the spin-independent DM-nucleus interactions are described using the standard astrophysical parameters for a Maxwellian velocity distribution [12] with an asymptotic velocity $v_0 = 220 \text{ km s}^{-1}$ and a galactic escape velocity $v_{\text{esc}} = 544 \text{ km s}^{-1}$, combined with a lab velocity $v_{\text{lab}} = 232 \text{ km s}^{-1}$. The local DM density is assumed to be $\rho_0 = 0.3 \text{ GeV c}^{-2} \text{cm}^{-3}$. The loss in coherence at high momentum is taken into account with the standard Helm form factor [13]. It is assumed that the cross-section scales as $A^2$, with $A$ being the mass number of the considered nucleus [14]. For a 100 MeV$c^{-2}$ WIMP, an induced nuclear recoil has less than 1 eV in energy, a quantity further reduced by some quenching factor, typically 0.1 at these low energies [15], whereas a Migdal electron yields a 100 eV signal. In order to avoid systematic uncertainties linked to the quenching factor, which is not properly measured for such low energy nuclear recoils [15], only the electronic contributions to the signal energy are considered in the following.

Because of the experiment underground location, the DM energy spectrum and flux will be modified by the action of the stopping power of the rock overburden [16–19]. These Earth-shielding effects were calculated using the publicly available verne code [20], introduced in [51]. A continuous energy loss of the DM particles is assumed through the atmosphere, the 1700 m rock overburden and the 20 cm lead shielding, as well as straight line trajectories [52]. Ref. [21] has shown that this simplified formalism gives rise to constraints similar to more complete Monte Carlo simulations.

For DM particles moving at low velocities, near the escape velocity at the Earth surface, $v_\text{earth} = 11 \text{ km s}^{-1}$, effects such as gravitational capture [53–55] and gravitational focusing [56] are not negligible. These effects are not taken into account in the flux calculation. Instead, the DM velocity distribution is conservatively set to zero below $v_{\text{cut}} = 20 \text{ km s}^{-1}$ when calculating the signal spectra. As in [14], the detector response to these calculated signals is simulated using the pulse simulation procedure presented in Sec. [11].

The signal occurs in a region of the spectrum where reliable background models are not available, as this is the first time that it is explored with the present detector technology. Therefore, the physics reach of this first prototype is estimated with a search limited to establishing the signal rate that is excluded at 90% C.L. by the observed spectrum using Poisson statistics, without any background subtraction. For each DM mass, the signal rate is calculated within a region of interest (RoI). This RoI is selected to maximize the sensitivity to the calculated signal of a hypothetical experiment, where the expected spectrum is taken as a smoothed version of the reference sample.

To reduce the effect of statistical fluctuations in the reference sample on the determination of the RoI, its energy spectrum has been smoothed using a sum of exponential functions together with a Gaussian peak to account for the presence of the 160 eV line from $^{71}$Ge neutron activation. A minimum width of 23 eV is imposed to the RoIs. The optimization of the RoIs is repeated for different values of the ionization energy criterion presented in Sec. [11] in order to achieve the best sensitivities. The optimized value for the criterion which improves up to a factor 3 the achieved limits is $E_{\text{ion}} > 400 \text{ eV}$, shown as the darkest green in Fig. [3]. With a large but acceptable statistical cost, the cut reduces the efficiency corrected rate by a factor 2 at 1 keV. Once RoIs are fixed for each DM-mass using the reference sample, the 90% C.L. upper limit on a possible Migdal signal is calculated using Poisson statistics, again considering that all events in the search data sample RoIs are potential DM candidates.

The resulting distributions for DM masses of 35 and 500 MeV$c^{-2}$ and the associated RoIs are shown in Fig. [5], where they are compared to the same experimental data as in Fig. [4] (presented in this case without the efficiency correction and in count per keV) on which is overlaid a smoothed model extracted from the independent reference sample (in blue). The model thus
includes a Gaussian peak at 3.7 keV (160 eV$_{ee}$) corresponding to the Ge M line. This shows how the signal drifts towards high energies for higher DM particle masses. The 90% C.L. limits are calculated for both the lowest excluded cross-section, but also for the highest cross-section for which Earth-Shielding would prevent the observation of a signal in the detector. These two types of excluded signals for a 50 MeV·c$^{-2}$ WIMP are shown with their associated ROIs in Fig. 6 in green for the upper part of the contour and in red for the lower one.

The extracted limits are shown in Fig. 7. The red contour (delimited by the thick red line) corresponds to the excluded cross-sections for WIMP masses from 32 MeV·c$^{-2}$ to 2 GeV·c$^{-2}$. The yellow and green bands correspond to the statistical uncertainties at 1 and 2σ determined using a Monte Carlo simulation randomly drawing events from the distributions of the signal and the smoothed reference. This shows that the red contour behaves as an expected fluctuation from our procedure with respect to the statistics of the search sample. The black line shows the 90% C.L. upper limit on the Migdal DM interaction for signal neglecting the effect from Earth shielding. The comparison with the red contour shows that these effects modify the rate and shape of the spectra for masses lower than 50 MeV·c$^{-2}$.

The 90% C.L. excluded region presented in Fig. 7 constrains masses down to 32 MeV·c$^{-2}$. Below this value of 32 MeV·c$^{-2}$, the very large cross-section needed to yield an observable signal leads to stopping effect from overburden and shielding, consequently, no constraint can be obtained for lower masses in this analysis. This contour is shown in Fig. 8 along with other experimental results [19, 20, 23, 29, 30, 57]. It constrains a new region of parameter space for cross-sections close to $10^{-29}$ cm$^2$ and masses between 32 and 100 MeV·c$^{-2}$. This contour is also compared to the previous results of an EDELWEISS-surf Migdal search [22] which was performed at the surface. Orders of magnitude of improvement have been achieved. The underground operation did not jeopardize the potential of this search, despite the enhanced Earth-shielding from the larger overburden, thanks to the significant reduction of the background level obtained in the EDELWEISS-III setup at LSM. The effective threshold of 30 eV$_{ee}$ achieved here, lower than the 60 eV threshold of Ref. [22], contributes to the extension of the search to masses below 45 MeV·c$^{-2}$. This threshold is more than five times lower than those of CDEX [23] (160 eV$_{ee}$) and XENON [20] (~200 eV$_{ee}$). However, both experiments achieved significantly better background levels, and this aspect is clearly the main limiting factor for the use of the present detector to probe lower cross-sections.
V. DISCUSSION

As the search for DM particles appears to be limited by backgrounds, these were investigated more thoroughly. It was found that most of the population in the energy interval between 0.8 to 3 keV come from events where a heat energy deposit is not associated with any ionization, since they are not affected by the NTL amplification. This is shown in Fig. 9 that compares the data recorded by NbSi209 at biases of 15 V and 66 V. The rise below 600 eV is mainly due to the read-out noise, which slightly increases at 66 V. The compatibility of the two spectra above 0.8 keV indicates that most events in that region are not affected by the NTL amplification. The fit of a power law ($\alpha E^\beta$) yields identical slopes within uncertainties to $\beta \sim 3.40$ for both spectra. This is further illustrated by the flatness of the ratio of the two spectra (bottom panel of Fig. 9) as a function of energy. The value of this ratio is $0.74 \pm 0.03$ (stat) $\pm 0.07$ (syst), where the central value is fitted in the range from 0.8 to 2.8 keV, and the systematic error considers variations of this range. This ratio depends on the fraction $x$ of events associated with charges. It should be equal to one for $x = 0$ in the absence of time-dependence of the rates [59]. The observed ratio is compatible with values deduced from the long-term variations observed at 15 V, but the deviation from 1 will be taken as a conservative systematic uncertainty associated to the time variations. Assuming a worst-case scenario where the HO and ER populations follow the same power spectrum, the resulting upper limit is $x < 0.0004$ at 90% C.L. This confirms that HO events dominate the spectra in the range from 0.8 to 2.8 keV.

At 66 V, this diagnostic concerns events with electron-equivalent energies between 25 and 130 eV$_{ee}$, well below what can be probed by the ionization signal resolution of 210 eV$_{ee}$. In these spectra, the cut on $E_{ion} > 400$ eV$_{ee}$ has been replaced by a cut on $E_{ion} < 0$ eV$_{ee}$ in order to accurately measure the contribution of HO events. Considering that the contribution of events with $E_{ion} < 0$ eV$_{ee}$ does not affect significantly the efficiency-corrected rates below 3 keV, it is a further indication that the HO population dominates the low-energy region.

The background rate after efficiency correction is $\sim 600$ events kg$^{-1}$ day$^{-1}$ keV$^{-1}$ at 1 keV, corresponding to $1.4 \times 10^3$ events kg$^{-1}$ day$^{-1}$ keV$^{-1}$ at 43 eV$_{ee}$ for the 66 V data. For comparison, Fig. 9 also shows the spectra observed in an EDELWEISS-surf 34 g de-
detector equipped with Ge-NTD heat sensors, operated above-ground at 0 V [22] and at LSM at 15 V [14]. In [14] [58], it was established by comparing data recorded at 15 V and 78 V that at LSM the 34 g detector spectrum was dominated by the HO background. In the energy range relevant for Migdal searches, i.e. above 30 eV_{ee} (690 eV), the backgrounds in NbSi209 are lower than those of Ref. [14], showing that the present detector is better suited for this type of searches, in terms of HO event rates. The green line shows the spectrum of the EDELWEISS-surv experiment [22]. The comparatively higher rate highlights the reduction of backgrounds achieved underground in the EDELWEISS-III setup and the consequent gain in sensitivity.

Studies to better understand the origin of these still unexplained HO events are ongoing. This background not only affects EDELWEISS detector but is a limiting factor for numerous experiments in the direct DM search cryogenic community [59]. Although the HO event rate per unit mass appears to be reduced relative to those observed in a smaller detector equipped with an NTD sensor, the change of sensor technology (with different sensitivities to thermal and out-of-equilibrium phonons) does not eliminate this type of events entirely. This excludes, for example, stress due to the gluing of the Ge-NTD as being the dominant cause of HO events.

VI. CONCLUSION

The EDELWEISS collaboration has searched for DM particle interaction exploiting the Migdal effect with masses between 32 MeV·c^{-2} and 2 GeV·c^{-2} using a 200 g Ge detector operated underground at the Laboratoire Souterrain de Modane. The phonon signal was read out using a Transition Edge Sensor made of a NbSi thin film. The detector was biased at 66 V in order to benefit from NTL amplification and resulting in a resolution on the energy of electron recoils of 4.46 eV_{ee} (RMS). The effective analysis threshold of 30 eV_{ee} is better than other Migdal searches, but is limited by a large background not associated to charge creation in the detector, whose cause remains to be identified. The search constrains a new region of parameter space for cross-sections close to 10^{-29} cm² and masses between 32 and 100 MeV·c^{-2}. The reduction of threshold achieved with the NbSi sensor shows the relevance of its use for out-of-equilibrium phonon sensitive devices for low-mass DM searches. In the context of its EDELWEISS-SubGeV program, the collaboration is also investigating new methods to significantly reduce HO backgrounds by improving its ionization resolution with the use of new cold preamplifiers [60], and by developing NbSi-instrumented devices able to tag the out-of-equilibrium NTL phonons associated to a single electron.

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