Quantitative optimization of emergency department's nurses of an educational hospital: a case study

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Abstract

Introduction: Nurses account for the majority of human resources in hospitals, as such that 62% of the workforce and 36% of hospital expenditures are related to nurses. Considering its vital role in offering round-the-clock emergency healthcare services, an Emergency Department (ED) requires adequate nurses. Therefore, this study was conducted to optimize the number of nurses in ED.

Methods: This was an applied study conducted using a Linear Programming (LP) model in 2015. The study population were selected by census who were all ED nurses (n=84) and patients referred to ED (n=3342). To obtain the statistics related to the number of patients and nurses, the hospital information system and human resources database were employed respectively. To determine the optimum number of nurses per shift, LP model was created via literature review and expert advice, and it was executed in WinQSB software.

Results: Before implementing the model, the number of nurses required for ED morning shift, evening shift, and night shift (2 shifts) was 26, 24 and 34 respectively. The optimum number of nurses who worked in ED after running the model was 62 nurses, 17 in the morning shift, 17 in the evening shift and 28 in the night shift (2 shifts). This reduced to 60 nurses after conducting sensitivity analysis.

Conclusion: The estimated number of nurses using LP was less than the number of nurses working in ED. This discrepancy can be reduced by scientific understanding of factors affecting allocation and distribution of nurses in ED and flexible organization, to reach the optimal point.

Keywords: Emergency Department; Nurses; Quantitative Optimization; Linear Programming Model

1. Introduction

Since the early 21st century, the role of Human Resources (HR) in the health system has been recognized by international organizations such as the World Health Organization (1). Specialized and trained HR is the heart of any health system that ensures its life and survival (2). In this regard, providing specialized HR in hospitals as the most pragmatic unit of health system (3) is of special importance, since it accounts for 50 to 80% of expenditures in this sector (4). Nurses often account for the major part of HR in hospitals (5), such that Dehghan, cited by Eastaugh has regarded 62% of hospitals’ HR and 36% of its expenditures related to nursing staff (6). This group plays a major role in promotion of health in society, without whom the hospitals will not achieve their goals (5). Of sectors, the success of which depends on having efficient and vigorous nurses along with other medical staff, is the Emergency Department (ED) which is an essential and inevitable element of hospitals considering its vital role in providing...
immediate medical care for patients who require quick intervention at all times of the day (7). Due to the critical
condition of patients referring to ED and hospitalization of over 28% of them in various wards of a hospital, the
quality of services provided in this department is regarded as a symbol of the general state of services provided in
the hospital (8). Providing suitable and programmed HR, namely nursing staff for ED is definitely one of the major
tasks of hospital administrators who should employ orderly and rational processes and systemic approaches to avoid
shortage or surplus (9); since, on the one hand, hospitals encounter resource constraints and rising costs, and on the
other hand, they should be accountable to medical requirements of patients and satisfy their expectations and
requirements (6). In this regard, since 1980, many authors have investigated scheduling of various medical staff,
including ED nurses, as such that the common objectives of all these studies are to determine the least number of
nurses required along with patients' satisfaction of emergency services provided, as well as to determine the number
of nurses required per shift (10). Within recent decades, various tools including statistics, work measurement,
simulation, queues and linear programming models have been used for scheduling problems of staff (11) as such
that within the last two decades, the use of simulation models for programming and decision-making in the health
sector has been extensively promoted and many of them have been used in the ED of hospitals (12). In 2009, Ahmed
and Alkhamis provided a tool to support decision-making using a simulation system along with optimization, to
determine the optimal number of physicians, laboratory technicians and nurses for a hospital in Kuwait, in order to
maximize the number of patients and reduce waiting time in ED, considering budget constraints. The main objective
of this tool was to evaluate the effect of optimal allocation of staff on efficiency of provided services. Results
showed that the use of optimization model results in a 28% increase in customers (patients) and a 40% decrease in
patients' waiting time (13). In this regard, various studies have demonstrated the appropriateness of a Linear
Programming (LP) model in optimal allocation of health system resources relative to other traditional methods. For
instance, Flessa (2000) and Beaulieu et al. (2000) employed this method respectively for optimal allocation of
resources in developing countries (14) and to schedule shifts for physicians and nurses in ED. Results from
employing this method showed a significant decrease in time and intended activity, and better scheduling in a 6-
month interval (15). This widely used model is a set of techniques and methods derived from mathematics and other
disciplines that is considerably effective in improving administrative decisions and finding optimal conditions and it
can suitably solve problems like production planning, allocation of limited resources and inquiry control. Managers
who are interested in the quality of their decisions' results, cannot be indifferent, relative to this issue (16). Relative
to other models including complex ones, this model is of more use due to being simple and feasible with data
available in EDs (11). The ED of the educational hospital under study in Bandar Abbas, as the largest ED in the
south of Iran, admits a high number of patients from all counties of the province and even adjacent provinces for
emergency services. Therefore, timely provision of these services, proportional to patients' needs, requires an
adequate number of trained nurses. In addition, since the LP model is one of the widely used optimization methods
for HR allocation proportional to the demand and workload, this study was conducted with the aim of estimating the
optimum number of nurses using the LP model in the ED of the intended hospital.

2. Material and Methods
This was an applied study, conducted using the quantitative technique of Linear Programming (LP). LP entails 3
main components of decision variables, objective function and constraints or limitations, and appropriate definition
of decision variables is the first major step to extend the model. Then objective function and constraints are
determined. Decision variables are those that values should be attributed to. Objective function shows the relations
between variables and objective of the problem and it seeks for optimization. Limitations are those constraints that
should be observed (17). This study was conducted using available data in 2015 when there was the high admission
rate of patients. Statistical population was selected taking a census including all patients (3,342 patients) referring to
the ED of the educational hospital in Bandar Abbas in the above-mentioned period as well as nurses working in this
ward (84 nurses). Data collection was conducted using the Hospital Information System (HIS) for the number of
patients, and the hospital HR database for data related to nurses. To verify the number of nurses working at ED
being up-to-date at the time of this study, data were reviewed by the nursing manager of the hospital. Furthermore,
confidentiality of obtained data was confirmed and they were used only for research purposes. Work shifts of the
hospital under study were designed as two 6-hour shifts (8 am to 2 pm and 2 pm to 8 pm) and a 12-hour shift (8 pm
to 8 am). To determine the mean admission of patients with sufficient validity and planning of the LP model, a 24-
hour period of this ward was divided into eight periods of 3-hours according to Table 1. According to the study by
Ketabi and Monzavi (11), patients referring to ED require one of low, medium and high levels of care and duration
of nursing services for each one of these levels is respectively 10, 20 and 45 minutes. On average, in each period,
40% of patients require low level nursing services, 20% need medium level and 40% need high level nursing
services. To determine the optimum number of nurses for ED per various shifts of the hospital, data entered Excel
software and descriptive statistics indices were extracted. To design the LP model, the initial model was extracted using literature review and it was finalized by specialized counseling. Then, using collected field data, the model was executed in WinQSB software. This software is among the simplest and yet the most accurate of engineering software able to solve various problems in a simple environment as a software package, by easy data entry, various solving methods, analyzing all parameters and understandable output (11).

### Table 1. Current eight shifts of the ED

| Current shifts of the ED | Division of eight shifts in ED |
|-------------------------|-------------------------------|
| Shifts | Period | Shifts | Period |
| First | 8 am-2 pm | First | 8 am-11 am |
| | | Second | 11 am-2 pm |
| Second | 2 pm-8 pm | Third | 2 pm-5 pm |
| | | Fourth | 5 pm-8 pm |
| Third | 8 pm-8 am | Fifth | 8 pm-11 pm |
| | | Sixth | 11 pm-2 am |
| | | Seventh | 2 am-5 am |
| | | Eighth | 5 am-8 am |

### 3. Results

The number of patients referring to ED within the study period was 3,342, and average admission of patients was 1,114. Considering the average number of customers in 3-hour shifts as well as the time required to supply nursing services for each group of patients (low, medium and high level care), and the percentage of patients who received low, medium and high level care, the number of nurses required to supply services for customers was obtained for each hour in Table 2.

### Table 2. Time served, the number of patients, and nurses required at any shifts of the ED

| Shifts | Period | Total number of patients referred in studied period | Average number of patients per shift | Nursing services required (min) | Number of nurses needed per shift |
|--------|--------|--------------------------------------------------|-------------------------------------|---------------------------------|----------------------------------|
| First  | 8 am-11 am | 360 | 40 | 1040 | 17 |
| Second | 11 am-2 pm | 732 | 81 | 2106 | 35 |
| Third  | 2 pm-5 pm | 360 | 40 | 1040 | 17 |
| Fourth | 5 pm-8 pm | 480 | 53 | 1378 | 23 |
| Fifth  | 8 pm-11 pm | 300 | 33 | 858 | 14 |
| Sixth  | 11 pm-2 am | 135 | 15 | 390 | 6 |
| Seventh | 2 am-5 am | 150 | 17 | 442 | 7 |
| Eighth | 5 am-8 am | 825 | 92 | 2392 | 40 |

The above-mentioned cases were used as the input for the LP model. The objective function of this model was the minimum number of nurses required for the ED of the hospital. In addition, the objective function, decision variables and constraints are as follows:

#### a) Objective function:

$$\text{Min } Z = X_1 + X_2 + X_3 + X_4 + X_5 + X_6 + X_7 + X_8$$

To determine decision variables, it is necessary to note that according to current shift schedule of the hospital as well as the times of this model, each shift can have nurses of various times, such that the morning shift (8 am-2 pm) could have nurses from the first period (8 am-11 am) and the second period (11 am-2 pm). In evening shift (2 pm-8 pm), it was possible to have nurses from the third (2 pm-5 pm) and fourth (5 pm-8 pm) periods. Furthermore, the night shift (8 pm-8 am) could entail nurses from fifth (8 pm-11 pm), sixth (11 pm-2 am), seventh (2 am-5 am) and eighth (5 am-8 am) periods.

#### b) Decision variables of above model were as follows:

- X1: The number of nurses whose shift started at 8 am.
- X2: The number of nurses whose shift started at 11 am (null).
- X3: The number of nurses whose shift started at 2 pm.
- X4: The number of nurses whose shift started at 5 pm (null).
- X5: The number of nurses whose shift started at 8 pm.
- X6: The number of nurses whose shift started at 11 pm (null).
X7: The number of nurses whose shift started at 2 am (null).
X8: The number of nurses whose shift started at 5 am (null).
c) Constraints:
c.1. Time-constraints (demand): According to these constraints, the number of nurses required for each period was as follows:
X1 ≥ 17
X1 + X2 ≥ 35
X3 ≥ 17
X3 + X4 ≥ 23
X5 ≥ 14
X5 + X6 ≥ 6
X5 + X6 + X7 ≥ 7
X5 + X6 + X7 + X8 ≥ 40
c.2. Supply constraints: This hospital encountered no constraints for supplying nurses in various work shifts.
c.3. Constraints of non-negative variables:
X1, X2, X3, X4, X5, X6, X7, X8 ≥ 0

After solving the model in WinQSB software, the optimum number of nurses required for ED in three work shifts of the hospital was 48 nurses (Table 3) and considering that the third shift is a 12-hour shift, the actual number of nurses required for a 24-hour cycle was (48+14)=62 nurses.

Table 3. The number of nurses required per shift in the ED of the hospital before and after running the model

| Shifts                  | Number of nurses needed before running the model | Number of nurses needed after running the model |
|-------------------------|-----------------------------------------------|-----------------------------------------------|
| First (8 am-2 pm)       | 26                                            | 17                                            |
| Second (2 pm-8 pm)      | 24                                            | 17                                            |
| Third                   | 17+17                                         | 14+14                                         |
| Total number of nurses  | 84                                            | 62                                            |

If the current shifts of the hospitals are changeable and nurses are allowed to start their work in various shifts, a lower number of nurses will be required due to fewer constraints. In other words, in the solved model, since the third shift starts at 8 pm and continues to 8 am, 14 nurses whose presence is required from 8 pm to 11 pm are practically at work until 8 am and the cost of their surplus is imposed to the hospital. However, if nurses can start work from the middle of current shifts, in the case of re-solving the LP model, the number of nurses required for every shift and the objective function will change as follows:
a) Objective function
Min Z = X1 + X2 + X3 + X4 + X5 + X6 + X7 + X8
b) Decision variables
X1: The number of nurses whose shift started at 5 am.
X2: The number of nurses whose shift started at 8 am.
X3: The number of nurses whose shift started at 11 am.
X4: The number of nurses whose shift started at 2 pm.
X5: The number of nurses whose shift started at 5 pm.
X6: The number of nurses whose shift started at 8 pm.
X7: The number of nurses whose shift started at 11 pm.
X8: The number of nurses whose shift started at 2 am.
c) Constraints:
c.1. Constraints of time (demand):
Based on these constraints, the number of nurses required in each time was as follows, based on new work shifts:
X8 + X1 ≥ 17
X1 + X2 ≥ 17
X2 + X3 ≥ 35
X3 + X4 ≥ 17
X4 + X5 ≥ 23
X5 + X6 ≥ 14
X6+X7 ≥ 6
X7+X8 ≥ 7

c.2. Supply constraints: None of the nurses were willing to start working at 2 am, X8=0.

c.3. Constraints of non-negative variables:
X1, X2, X3, X4, X5, X6, X7, X8 ≥ 0
X1=17, X2=0, X3=17, X4=0, X5=14, X6=6, X7=6

In addition, the least number of nurses required at this state was z=60 that compared to previous state, 2 fewer nurses were required.

4. Discussion

Determining the optimum number of human resources in EDs of hospitals has been investigated in several studies (11, 18-20). Based on results of these studies, considering the importance of this ward and the emergency nature of its functions, absence of an optimum number of human resources can directly affect the quality of activities performed in this ward as well as patients' satisfaction. Low number of human resources, namely nurses, can disrupt the quality and quantity of services provided in this ward, and result in crowding of patients and lack of receiving timely care. On the other hand, an excess number of nurses will result in imposition of excess expenses to the hospital and in addition, will make organization and coordination of them more difficult (19, 20). Therefore, determining the optimum number of nurses is the main task of managers in this ward, and this study confirmed that its importance was similar to other studies. In this study, using an LP model, the optimum number of nurses was estimated to be 62. This value in Ketabi's study was 36 nurses, in Sotodezadeh it was seven and in Bayati's study it was three (11, 18, 21). The estimated number of nurses in these studies is different depending on the type and size of the hospital, as well as the number of referring patients. In this study, this number is higher compared to similar studies, since the hospital under study is the largest hospital in the province and many patients from all over the province refer or are referred to the ED of this hospital. Considering the number of nurses working in this ward (84 nurses), 22 are determined as extra forces. This number is higher than the optimum value and it clearly imposes extra expenses to the hospital. Centeno (2003) who had employed simulation and LP in combination to determine the optimum number of ED nurses, showed that the number of nurses estimated, using these methods, is lower compared to the number of nurses calculated experimentally (10), which complies with the results of present study. Current hospital shifts impose many constraints in determining the optimum number of nurses. In this regard, by changing the number of shifts, the start point of each shift and its duration, employing sensitivity analysis in various studies including the present study, has sought to reduce these constraints to employ a variable number of nurses in shorter shifts and this will reduce the total number of nurses. In sensitivity analysis, the estimated number of patients was lower compared to the estimated number resulted from the LP (11). This reduction in present study was two nurses and Ketabi's study shows a reduction in required workforce of up to eight nurses (11). Therefore, flexibility in organizing work shifts and creating a culture of acceptance among nurses working at ED can assist allocating the optimum number of nurses that, while they are quantitatively adequate for each shift, no damage is imposed to the quantity and quality of services provided. Like similar studies, results of this study showed that the LP model is employed as a practical model to determine the optimum number of nurses in many cases. In this regard, Ketabi stated that this model can not only determine the optimum number of nurses, but can also determine the number of nurses required for each work shift (11). However, this model suffers from some limitations including being single-objective and an inflexibility that disables groups' decision-making (22). Therefore, to solve optimization problems, including the optimum number of HR, it is suggested that an ideal programming model is used with the capability of selecting multi-objectives, flexibility in decision-making and considering preferences of various decision-making groups for multiple and sometimes contradictory objectives. Considering the lack of access to accurate data of all months of the year and selecting only some months, as well as lack of access to complete data to estimate the time required to provide nursing services, and using data from similar studies, this study encountered some limitations. To remove them, it was attempted to use data of the months with the highest number of customers based on which the highest number of nurses was estimated. In addition, data from a relatively similar study was employed, to determine the time of providing nursing services as well as modeling assumptions. Finally, it is suggested that accurate and complete data be provided, to create model assumptions according to the demands of the hospital and to employ flexible models to determine the optimum number of nurses.

5. Conclusions

In summary, findings of this study showed that the estimated number of patients using the LP model was much lower than nurses working at the ED of the hospital under study. The functional significance of these findings is that by using scientific understanding of factors affecting allocation and distribution of nurses in ED and their flexible...
organization, the number of nurses can reach the optimum value. Therefore, it is suggested to conduct shift scheduling using sensitivity analysis such that it is proportional to the demand of services in various hours of a day to satisfy demands and reduce the burden of HR expenses. Finally, conducting a complementary study for quantitative optimization of nurses in all clinical wards of the hospital can be a suitable course for future studies on this issue.

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Conflict of Interest:
There is no conflict of interest to be declared.

Authors' contributions:
All authors contributed to this project and article equally. All authors read and approved the final manuscript.

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