Performance simulation of a MRPC-based PET Imaging System

A. Banerjee, S. Chattopadhyay

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Abstract
The low cost and high resolution gas-based Multi-gap Resistive Plate Chamber (MRPC) opens a new possibility to find an efficient alternative detector for Time of Flight (TOF) based Positron Emission Tomography, where the sensitivity of the system depends largely on the time resolution of the detector. Suitable converters can be used to increase the efficiency of detection of photons from annihilation. In this work, we perform a detailed GEANT4 simulation to optimize the converter thickness thereby improving the efficiency of photon conversion. Also we have developed a Monte Carlo based simulation of MRPC response thereby obtaining the intrinsic time resolution of the detector, making it possible to simulate the final response of MRPC-based systems for PET imaging. The result of the cosmic ray test of a four-gap Bakelite-based MRPC operating in streamer mode is discussed.

1 Introduction

Under Nuclear Medicine, Positron Emission Tomography (PET) is an important imaging technique in which a radio-pharmaceutical having positron emitter is injected into the object of study. This radioactive element can be used to collect the morphological information from the object. Inside the object, these positrons annihilate with the available electrons to produce two nearly back-to-back photons each having energy of 511 keV. The simultaneous detection of these photons with efficient detectors can lead to the identification of annihilation point. As these positron emitters are injected via some physiological substances, mapping of the density of the positron sources can give the information about the activity inside the object of interest.

Although PET gives various important information which the other imaging techniques are not able to provide, limitations due to a short field of view (FOV) (∼16 cm in standard PET scanners), long dead time of the electronics among others affect the sensitivity and the spatial resolution of the currently available PET scanners. Moreover, to obtain an image, in a reasonable examination time a high radiation dose is required to deliver within the object to collect sufficient amount of data.

In a Time-of-Flight (TOF) PET scanner, the arrival times of each coincident pair of photons are more precisely known, and the (extremely small) difference between them is used to localize the annihilation event along the line between
the two detected photons. This additional TOF information helps to improve the image quality by reducing the length over which the coincident events are back-projected. Instead of being back-projected over the entire distance through the body, the events are back-projected over a smaller distance, determined by the timing resolution of the scanner. For example, for a coincidence timing resolution of 600 ps the positional uncertainty is 9 cm Full Width at Half Maximum along the line pair. The average diameter of a typical patient (torso) is 25 - 30 cm, or approximately three times the TOF positional uncertainty. The ratio of patient diameter (D) to the positional uncertainty (\( \Delta x \)) has been reported to be representative of the noise reduction, or the sensitivity gain, with TOF. This benefit in TOF increases as the PET system timing resolution improves.

The detectors that are generally used worldwide for PET imaging are the scintillator-based detectors, e.g., Bismuth germanate (BGO) or Lutetium orthosilicate (LSO), as they have excellent light output and very good energy resolution. But because of its high cost and the above-said limitations, several attempts are being made to find an alternative. Multi-gap Resistive Plate Chambers (MRPCs) are considered to be a good alternative to the scintillator-based PET imaging systems because of their excellent time resolution (~ 50 ps) and position (~ 1 mm) resolution in addition to the relatively lower cost of fabrication. In MRPC-based system, the location of the origin of photons can be obtained in 3-dimensions. The detector cell provides the position in transverse plane (x-y plane) and the time of arrival on the detector gives the distance in z-direction. If the time resolution of the MRPC is known then an estimation of the spread for the position of origin of photon source can be obtained by the formula [1]:

\[
\Delta L [\text{mm}] \approx \frac{\sigma_t [\text{ps}]}{2}
\]

where \( \Delta L \) is the FWHM in the position accuracy and \( \sigma_t \) is the rms time accuracy per photon. Reconstruction of events however improves the resolution thereby producing the desired image granularity (few mm).

Several attempts have been made in building MRPC-based prototype PET imaging systems using varying number of gaps. However, like many other gas-based detector systems, the efficiency of conversion of 511 keV photons is very low. MRPC, due to its layered structure, has a natural configuration where proper conversion materials can be placed to obtain better efficiency. However, very thick converter will likely to absorb the produced electrons before they can reach the gas volume, whereas for very thin one it is very difficult to have a good conversion efficiency. Efforts have been made to optimize the converter-MRPC combination for obtaining best possible efficiency of single 511 keV photon detection. A maximum value up to ~ 20-25% has been reported, as mentioned in Ref [1][4].

In this work, we have performed a detailed simulation to optimize the detection efficiency of a pair of 511 keV photons likely to be generated from positron annihilation. The work includes the response of the passage of the photons inside the material by GEANT4 and a Monte-Carlo (MC) based simulation package for obtaining the MRPC signals giving their timing properties due to produced electrons. The simulation is done in two stages. First, GEANT4 has been used to simulate the conversion of the incident photons. The electrons obtained by photon conversion are considered to be the particles ionizing the
The processes for ionization to signal generation have been implemented in another MC code.

We organize the article as follows. In Sec. 2, we discuss the simulation procedure, in Sec. 3 we give the results obtained from the simulation and in Sec. 4 we present the results of the performance of a four gap Bakelite-base MRPC, operated in streamer mode.

2 Simulation Procedure

2.1 Conversion of 511 keV photons

GEANT4 (version 4.9.4) has been used to simulate the response of photons through the detector thereby generating electrons which reach the gas volume. GEANT4 [6, 7] is the efficient toolkit where different aspects of simulation process, such as the geometry of the system, the materials involved, the generation of secondary particles, the tracking of particles through materials, the physics processes governing particle interactions, the response of sensitive detector components, etc. can be implemented. For gamma ray conversion, the data file G4EMLOW version 6.19, containing cross-sections for low energy electromagnetic processes, was used.

The photon-pairs are considered to be back to back lying on the same plane. For attaining good conversion efficiency, we have used a set of Lead-MRPC combinations as shown schematically in Fig. 1. Two such combinations are placed facing each other considering the source of photon-pair to be in between as shown in Fig. 1. In this work, as an input of GEANT4, we have used different materials including lead as the converter, glass as detector material and the mixture C₂F₄H₂/i-C₄H₁₀/SF₆(85/5/10) as the gas volume in the gas gap. We have studied the variation of the conversion efficiency by varying the converter thickness.

Figure 1: Schematic representation of the detector configuration

Two photons with momenta of same magnitude (511 keV) but opposite directions are used as the input for every event. Any particle (photon or electrons) backscattered from one detector to the other are not considered for further
study. Photons get converted mainly in the lead volume mostly by the Compton and the photoelectric processes [1, 2]. A number of low energy electrons get absorbed inside the lead volume. Only the electrons reaching any one of the gas volume are considered for signal generation. Increasing the number of Pb-MRPC combinations improves the conversion probability, which subsequently decreases due to the absorption of electrons. The conversion efficiency of each detector is defined as the ratio of the number of the photons that generate electrons after conversion in any of the gas gaps to the number of the incident photons.

2.2 Monte Carlo study for response of MRPC

The conversion electrons resulting from GEANT4 are used as the input to the Monte-Carlo based programme, developed to study the response in the gas volume for signal generation. When the electron passes through the gas volume it ionizes the gas, which leads to the avalanche formation. During primary ionization the average number of clusters formed into the gas mixture is considered to be around nine/0.2 mm [2], which is the higher for slow electrons from converted photons than the value commonly used for minimum ionizing particles for the gas of given composition. The avalanche development from the primary cluster within the gas volume is governed by the Townsend coefficient ($\alpha$) and the attachment coefficient ($\eta$), which in this work are simulated by HEED [8].

The probability to obtain $n$ avalanche electrons at position $x$ within the gas volume, considering the electrode to be at $x=0$, is given by the relation [9]

$$P(n, x) = \begin{cases} \frac{\eta(x) - 1}{\eta(x) - k}, & n = 0 \\ \eta(x)^2 \left( \frac{\eta(x) - 1}{\eta(x) - k} \right)^{n-1}, & n > 0 \end{cases}$$

(2)

where $\eta(x) = e^{(\alpha - \eta)x}$ and $k = \frac{2}{\gamma}$.

To reduce the computational time in avalanche formation by a large number of secondary electrons, in our case for $\eta(x) > 200$, we have used the Central Limit Theorem (CLT), as mentioned in Ref [9], to obtain the average number of electrons and their spread after avalanche at a particular position. The space charge effect is also implemented by the application of a cut off on the number of avalanche electrons, after which multiplication stops. In the present case, the threshold applied is $1.6 \times 10^7$. Finally the avalanche electrons induce current signals onto the MRPC pick-up strips. The particle is said to be detected if the induced charge crosses a threshold value, which is 20 fC in our case. The detection efficiency of the MRPC, in this work, is defined as the ratio of the number of particles crossing the threshold charge value to the number of converted particles entering the gas gap. The concept of multi-gap has been implemented within the MC code by introducing a number of sub-gaps, keeping the total width of the gas volume same.

During this study, we have simulated the detection efficiency and the time response of MRPC for varying number of gaps. No effort has been made to implement the response of the readout electronics. We have defined the avalanche growth time as the time taken by the avalanche, starting from time $t=0$, to
produce sufficient number of electrons within the gas volume so that it can induce a charge greater than 20 fC to the MRPC electrodes. The standard deviation of the distribution of the avalanche growth time taken over a large number of particles is called the time resolution (TR) of the detector for single photon. For a pair of detectors, facing each other, as shown in Fig. 1., the difference of the time \( t_1 \) taken by one photon to produce a detectable avalanche in one detector and the time \( t_2 \) taken by the other photon to produce the same in another detector is defined as the pair time difference \( \delta t = t_1 - t_2 \). The standard deviation of pair time difference taken over a large number of photon pairs is defined as pair time resolution (PTR) for pair of photons. For the case, when both the detectors are equally spaced from the point of origin of the photon pair, PTR is governed mainly by the folding of TR of two detectors.

3 Simulation Results

3.1 Efficiency of photon conversion

The conversion efficiency is already defined in the previous section. Fig. 2 shows the conversion efficiency over the number of gas gap, where we have varied the converter thickness. By increasing the number of gaps, the effective thickness increases. It is seen clearly that with increasing number of gaps, the conversion efficiency increases. However for larger thickness, e.g. 0.1 mm, etc., the efficiency does not go higher than 18% thereby suggesting the converted electrons to stop inside the lead volume. Use of thinner converter in large numbers however increases the efficiency even further. The plot indicates that an efficiency \( \geq 25\% \) can be achieved with a configuration having 120 gaps, the converter thickness being 0.002 cm. From the plot it can be seen that the converter having thickness 0.0008 cm is also giving an impressive conversion efficiency beyond 140 layers. A saturation of the conversion efficiency for more
than 140 gaps is observed for almost all the converter thickness studied. It is of utmost importance to optimize the converter thickness for having a good conversion efficiency. During all through our study we have considered the optimized converter thickness as 0.004 cm.

Fig. 3 indicates the photon conversion efficiency with the configuration prescribed earlier for different materials each having the same thickness of 0.004 cm. The plot clearly indicates that lead is the most suitable converter for 511 keV photons for 0.004 cm thickness of the converter layer.

![Conversion efficiency as a function of number of gaps](image)

**Figure 3:** Conversion efficiency as a function of number of gaps

We therefore conclude that a suitable tuning of converter material and thickness can help to achieve reasonable conversion efficiency in a multi-gap configuration.

### 3.2 Time response for MRPC

In Fig. 4 we have plotted the distribution of the signal collection time for single photon incident on the detector having 20 gas gaps as obtained from MC simulation for MRPC response. The total number of entries in this plot indicate the total number of the particles after conversion. The time resolution ($\sigma$) is found to be $\sim 17$ ps, which is in good agreement with earlier results [10].

The pair time resolution was calculated considering the start time to be zero. Fig. 5 shows the distribution of the pair time difference collected from both the detectors. The standard deviation of the plot, 24 ps in this case, has a good agreement with the fact that both the detector have the same intrinsic time resolution.

We have observed the effect of the number of gaps in time resolution by varying the number of the gas gaps, keeping the total width of the gas gap to be the same. It is seen that the time resolution decreases with the number of gas gaps.
3.3 Estimation of the position resolution for an extended source of photon pairs

In this work, we have also estimated the position resolution of the detector in the prescribed configuration for an extended annihilation source. For this purpose, we have introduced a Gaussian spread of the source position in one direction, e.g., in z-direction keeping mean at zero and sigma of 0.5 mm. The photon pairs are back to back on same plane. We have then obtained the corresponding time difference measured by the pair of detectors. In Fig. 6 we have plotted the ratio of the distance of the source from the origin to the corresponding measured time difference. The spread gives an estimation of the resolution of the position measurement.

In this case the time of detection of a photon by the detectors is the sum of the time taken by the photon to reach the detector from the point of its origin and the signal generation time for each detector. It should be mentioned that the contribution from the second plays the leading role in the spread of the
Figure 6: Ratio of the distance of the point of generation for the origin to the photon detection time by the system detection time.

4 Performance of the prototype MRPC

The RPC technology mentioned in [11,12] was used to build a four-gap Bakelite-based MRPC. Bakelite plates of 30 cm × 30 cm in dimension and thickness of 1.2 mm had been used as electrodes and a uniform spacing of 0.6 mm each had been maintained by a high resistive material G-10 (resistivity ∼ 10^{13}Ω-cm). A mixture of Ar/i-butane/Freon(R134a) in the ratio of 55/7.5/37.5 was used as the working gas. A very thin coating of Silicone has been applied on the inner surfaces of the Bakelite plates to improve the surface roughness. The detector has been operated in streamer mode as it gives larger signal size and does not need any preamplifier. The detector has been tested with cosmic muons using the signals from three scintillators for trigger. Even though for these application, glass-based detectors operating in avalanche mode are usually used, the performance of 4-gap Bakelite-based detector will provide the lower limit of resolution for a least expensive option of background filtering PET imaging. Fig. 7 shows the efficiency as a function of the high voltage. An efficiency plateau 95% had been obtained for an applied high voltage greater than 13.5 kV. The distribution of the time difference between the master trigger and the signal from one MRPC strip is shown in Fig. 8. From the time difference spectrum, the full width at half maximum (FWHM) and the corresponding standard deviation (σij), where i and j refer to scintillators and the MRPC, were obtained by fitting a gaussian function. σij’s were similarly obtained for 3 different pairs of the scintillators, taking START signal from one and STOP signal from the other. The intrinsic time resolutions of the MRPC and the scintillators were obtained from the individual standard deviations σi, σj, which were extracted by solving the equation: σij^2 = σi^2 + σj^2.

The variation of FWHM and the time delay for the MRPC is shown in Fig.
The extracted time resolution ($\sigma$) of the MRPC at 14 kV operating voltage for a typical run was found to be $\sim 870 \pm 0.03$ ns.

5 Conclusions and outlook

MRPC-based PET system is potentially an attractive alternative to the scintillator-based system. In this work we have performed detailed simulation for the detection of photon pairs for MRPC-based system. A layered structure of MRPC with thickness 0.004 cm lead converter can give conversion efficiency greater than 25%, which is higher compare to normally available values for gas detector.
systems. For a 20 gap system, time resolution of photon pair can reach upto 17 ps. We have also performed simulation for the position measurement for an extended source of 500 µm width and found that the spread of the photon source can be measured with the addition of 3.17% extra fluctuation. This suggests the appreciability of these systems for measurements of photon-pair position to micron level.

As an effort to obtain a least expensive PET imaging system capable of filtering the background, we have built a 4-gap Bakelite-based MRPC giving time resolution of $\sim 900$ ps. For applications requiring relatively lower resolution, such a system can be useful. This also provides a platform to build a full glass-based high resolution MRPC system for PET imaging.

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