1. INTRODUCTION

A huge number of studies have been devoted to categorize neurons in the brain according to various criteria such as morphology, physiology, biochemical properties and synaptic characteristics (Peters et al., 1984; White, 1989; Cauli et al., 1997; Toledo-Rodriguez et al., 2003). However, relatively little has been said about their classification in terms of energy demands. The relationship between the action potentials characteristics and the energy cost required to generate them has been reported recently (Crotty et al., 2006; Carter and Bean, 2009; Sengupta et al., 2010). Nonetheless, as in many other works, the calculations of the metabolic energy involved in the generation of action potentials are based on the ion-counting methods that generally focus on the number of ATP molecules hydrolyzed by the sodium pump.

It is well known that Na\(^+\) and K\(^+\) are the most important ions with greater impact on the membrane potential dynamics and on its energetics (Ames III, 2000). In fact, these two ions together with Ca\(^{2+}\) account for the major ions whose movements consume ATP molecules. During the generation of action potentials, the electrochemical gradients are partially altered and must be restored by Na\(^+\)/K\(^+\) pump which mediates influx of 2 K\(^+\) in exchange for 3 Na\(^+\) per 1 ATP molecule consumed (Kandel et al., 1991). Estimations of the energy consumed by the neuron during its signaling activity are usually intended by extrapolating from a Hodgkin–Huxley type model the number of sodium ions required to depolarize the membrane in order to know the amount of ATP molecules that will be needed for the pump to reestablish its rest potential. This method, known as ion counting approach, corresponds to the first approach to account with the neuron energy (Laughlin et al, 1998; Attwell and Laughlin, 2001; Alle et al., 2009). Taking into account that action potential propagation following Hodgkin/Huxley kinetics is based on equal Na\(^+\) efflux and K\(^+\) influx, this approach could lead to overestimate/underestimate values of energy (Hertz et al., 2013). For one hand, because of the asymmetry between Na\(^+\), K\(^+\)-ATPase mediated Na\(^+\) and K\(^+\) fluxes. And, for the other hand, due to the overlap of inward and outward currents during an action potential generation. In fact, inward Na\(^+\) and outward K\(^+\) overlap during the action potential generation introducing an uncertainty in the calculation of sodium ions up to a factor of 4 (Hodgkin, 1975; Attwell and Laughlin, 2001; Lennie, 2003).

Based on computational models that capture the intrinsic properties of action potentials from different mammalian neurons, this work provides a quantitative comparison of the amount of ionic currents crossing the membrane during an action potential and their corresponding energy demands focusing on a new approach. This approach is based on the biophysical considerations about the nature of computational models used to account for neuronal spiking response, and gives an alternative method to deduce the electrochemical energy involved in the dynamics of the neuron model. Unlike the ion counting approach, this method requires no hypothesis about the stoichiometry of the ions or the extent of the overlapping between Na\(^+\) and K\(^+\) ions and, most
importantly, offers the possibility to compute the energy consumption of coupled neurons (Moujahid et al., 2010, 2011), especially when considering complex networks where all the interactions should be considered. As commented in Buzsáki et al. (2007) it is not possible to estimate energetic costs in isolation. As far as possible the complexity of the interactions should be taken into account.

The analytical expression of the electrochemical energy involved in the dynamics of the classical Hodgkin–Huxley model consisting of sodium, potassium and leakage currents has been reported previously in Moujahid et al. (2011, 2012). Here we provide energy functions of different spiking neurons where additional ionic currents are involved. The intrinsic properties of the computational models, considered in this work, arise from voltage-dependent conductances described by Hodgkin–Huxley type kinetics. These models were adjusted in previous studies (Wang and Buzsáki, 1996; Guo et al., 2008; Pospischil et al., 2008) to experimental data from different preparations to reproduce the firing characteristics of different neuron classes present in neocortex, thalamus and hippocampus. These neurons include regular spiking (RS) cells, fast spiking, intrinsically bursting (IB), hippocampal fast-spiking interneuron (HFI) and thalamocortical relay neuron (TCR). The RS and FS models can reproduce respectively firing properties of RS and FS cells as observed both in intracellular recordings of cells in ferret visual cortex and in rat somatosensory cortex. Meanwhile, IB neuron models reproduce the typical firings of intrinsically bursting cells in guinea-pig somatosensory cortex and in cat visual cortex. The other two neuron models capture the typical spiking as seen in rat hippocampal interneuron and a mouse thalamocortical relay neuron, respectively.

The paper is organized as follows. First, we introduce the dynamics and electrochemical energy of the Hodgkin–Huxley like models used to account for the spiking response of different classes of neurons present in neocortex, thalamus and hippocampus. Then we describe the kinetic of these neurons according to the ionic currents involved in their dynamics. Results are reported and discussed in section 3. Finally, section 4 draws conclusions and open questions.

2. MATERIALS AND METHODS

2.1. DYNAMICS OF THE SPIKING NEURON MODELS

All computational models were modeled using a Hodgkin–Huxley type of kinetic model (Hodgkin and Huxley, 1952), and run using the Matlab simulation environment. For all these models, the dynamics governing the membrane potential obeys the following equation:

$$C\dot{V} = -g_l(V - E_l) - I_{Na} - I_K - I_M - I_L - I_T + I_{Stim}. \tag{1}$$

where $V$ is the membrane potential in mV, $g_l$ is the maximal conductance per unit area for the leakage channel, and $E_l$ is the corresponding reversal potential. $I_{Stim}$ is the total membrane current density in $\mu A/cm^2$. $C$ is the membrane capacitance in ($\mu F/cm^2$). $I_{Na}$, $I_K$ ($I_M$), and $I_L$ ($I_T$) are the sodium, potassium (slow potassium) and calcium (low-threshold calcium) currents, respectively.

2.1.1. Neocortical neurons

In the models used to account for the different firing patterns characterizing cells in the neocortex, $I_{Na} = g_{Na}m^3h(V - E_{Na})$ and $I_K = g_Kn^4(V - E_K)$ are the sodium and potassium currents responsible for action potentials. $I_M = g_Mq(V - E_Ca)$ is a slow voltage-dependent potassium current responsible for spike-frequency adaptation, and $I_L = g_Lq^2r(V - E_Ca)$ is a calcium current to generate bursting.

The gating variables $m, h, n, q$ and $r$ obey the standard kinetic equation, $\dot{x} = \alpha_x(1 - x) - \beta_xx$, where $x = m, h, n, q, r$ and $\alpha_x$ and $\beta_x$ are voltage-dependent variables. $m$ and $h$ are potassium channels activation and deactivation variables, $n$ is potassium channels activation variable, and $q$ and $r$ are calcium activation and inactivation variables. The gating variable $p$ associated with the slow voltage-dependent potassium current is governed by the following equation: $\dot{p} = (p_\infty(V) - p)/\tau_p(V)$.

The RS model consists of the sodium and potassium currents responsible for action potentials ($I_{Na}$ and $I_K$) and a slow voltage-dependent potassium current responsible for spike-frequency adaptation ($I_M$). The IB model includes the same ionic currents as in the RS ones and an additional L-type calcium current ($I_L$). The simple FS model accounts only for the currents responsible of spike generation (i.e., $I_{Na}$ and $I_K$), and reproduces the spiking properties of FS cells as observed from ferret Visual Cortex in vitro. To capture the firing characteristics of FS cells as recorded from somatosensory cortex in vitro a slow potassium current ($I_M$) has been added to the simple FS model.

2.1.2. Thalamocortical relay neuron

The thalamocortical relay neuron model consists of currents responsible for generating spikes, $I_{Na} = g_{Na}m^3\alpha_x h(V - E_{Na})$ and $I_K = g_K(0.75(1 - h))^4(V - E_K)$, as well as, low-threshold calcium current, $I_T = g_T\alpha_x^2n(V - E_T)$. The dynamics of the gating variables $h$ and $r$ obey respectively the equations $\dot{h} = (h_\infty - h)/\tau_h$ and $\dot{r} = (r_\infty - r)/\tau_r$. This model achieves a single spike activity consisting of trains of action potentials whose frequency depends on the strength of depolarization. When exposed to depolarizing current pulse of constant amplitude it results in a train of action potentials with no frequency adaptation.

2.1.3. Hippocampal interneuron

Finally, the hippocampal interneuron model obeys the same current-balance equation (Equation 1), and consists of leak current and the spike-generating Na$^+$ and K$^+$ voltage-dependent ion current ($I_{Na} = g_{Na}m^3h(V - E_{Na})$ and $I_K = g_Kn^4(V - E_K)$). For the transient sodium current, the activation variable $m$ is assumed fast and substituted by its steady-state function $m_\infty = \alpha_m/\alpha_m + \beta_m$. This model has the ability to reproduce repetitive spikes at high frequencies in response to a constant injected current. It has a small current threshold (the rheobase $I_{stim} < 0.25 \mu A/cm^2$), and the firing rate is as high as 400 Hz for $I_{stim} = 20 \mu A/cm^2$.

In this work, we use the conductance-based model by Pospischil et al. (2008) to reproduce the main features of the typical firing pattern of RS, FS and IB neurons as observed in different cells in the neocortex. The computational models used to account for the firing characteristics of thalamocortical relay neuron and the hippocampal fast-spiking interneurons follow respectively the
works by Wang and Buzsáki (1996), Sohal et al. (2002), and Guo et al. (2008). The forms of the activation and inactivation functions describing the ion currents of all these models are reported in Table 1. The values of biophysical parameters characterizing each of these models are shown in Table 2, and give rise to 10 different cells. Cell 1 is a RS cell from ferret visual cortex, Cells 2 and 3 are respectively excitatory and inhibitory RS cells from a rat somatosensory cortex, Cells 4 and 5 are respectively FS cells from ferret visual cortex and rat somatosensory cortex, Cells 6 and 7 are both IB cells from guinea-pig somatosensory cortex (Cell 6 is characterized by an initial burst followed by adaptive action potentials, while Cell 7 gives rise to repetitive bursting), Cell 8 is an IB cell from a cat visual cortex, Cell 9 is a mouse thalamocortical relay cell, and finally Cell 10 account for a rat hippocampal interneuron.

### 2.2. IONIC CHANNELS ENERGY IN SPIKING NEURON MODELS

The procedure followed to find the electrochemical energy involved in the dynamics of the Hodgkin–Huxley circuit consisting of capacitor $C$ and three $Na$, $K$, and $L$ ionic channels has been reported in detail in Moujahid et al. (2011). Here we extend this procedure to deduce the energy functions characterizing the dynamics of Hodgkin–Huxley-like models where additional ionic channels are present. For the system given by Equation (1), the total electrical energy accumulated in the circuit at a given moment in time is,

$$ H(t) = \frac{1}{2} CV^2 + H_I + H_{Na} + H_K + H_M + H_L + H_T. $$

where the first term in the summation gives the electrical energy accumulated in the capacitor and represents the energy needed to create the membrane potential $V$ of the neuron. The other six terms are the respective energies in the batteries needed to create the concentration jumps in chloride, sodium, potassium and calcium. The electrochemical energy accumulated in the batteries is unknown. Nevertheless, the rate of electrical energy provided to the circuit by a battery is known to be the electrical current through the battery times its electromotive force.

### Table 1 | The activation and inactivation functions describing ion currents.

| Activation | Inactivation |
|------------|-------------|
| **NEOCORTICAL CELLS** | |
| $I_{Na} = g_{Na}m^3h(V - E_{Na})$ | $\alpha_n(V) = \frac{-0.32(V - V_I - 13)}{\exp(-(V - V_I - 13)/4) - 1}$ |
| | $\alpha_h(V) = \frac{0.128\exp(-0.068(V - V_T - 17)/18)}{\exp(-0.068(V - V_T - 17)/18) - 1}$ |
| | $\beta_m(V) = 0.28\exp(V - V_T - 40) / (\exp(V - V_T - 40) - 1)$ |
| | $\beta_h(V) = \frac{4}{\exp(-0.068(V - V_T - 17)/18) + 1}$ |
| $I_K = g_Kn^4(V - E_K)$ | $\alpha_n(V) = \frac{-0.032(V - V_I - 15)}{\exp(-(V - V_I - 15)/5) - 1}$ |
| | $\alpha_m(V) = \frac{0.00457\exp(-0.13 - V)/50}{\exp(-0.13 - V)/50 - 1}$ |
| | $\beta_q(V) = \frac{0.94e^{-V_T}/17}{\exp(-V_T)/17 + 1}$ |
| $I_L = g_Lr^2(V - E_{L_C})$ | $\alpha_n(V) = \frac{1}{\exp(-V + 35)/10 + 1}$ |
| | $\tau_p(V) = \frac{\tau_{max}}{3.3e^{(V + 35)/20} + \exp(-V + 35)/20}$ |
| | $\tau_{max}(V) = 1/(e^{(V + 37)/7} + 1)$ |
| **THALAMOCORTICAL RELAY (TCR) CELL** | |
| $I_{Na} = g_{Na}m^2h(V - E_{Na})$ | $m_{Na}(V) = 1/(e^{-(V + 37)/7} + 1)$ |
| | $h_{Na}(V) = 1/(e^{(V + 41)/4} + 1)$ |
| $I_K = g_K(0.75(1 - h))^4(V - E_K)$ | $\tau_\lambda(V) = 1/(\alpha(V) + \beta_1(V))$ |
| | $\alpha_1(V) = 0.128\exp(-V + 46)/18$ |
| | $\beta_1(V) = 4/(1 + \exp(-V + 23)/5)$ |
| $I_L = g_Lr^2(V - E_L)$ | $\tau_\lambda(V) = 1/(e^{(V + 84)/4} + 1)$ |
| | $\tau_{L}(V) = 0.4(\exp(-V + 25)/10.5 + 28)$ |
| **HIPPOCAMPAL INTERNEURON (RHI)** | |
| $I_{Na} = g_{Na}m^2h(V - E_{Na})$ | $m_{Na}(V) = \frac{\alpha_n(V)}{(\alpha_n(V) + \beta_m(V))}$ |
| | $\alpha_n(V) = \frac{-0.1(V + 35)}{\exp(-0.1(V + 35)/30) - 1}$ |
| | $\alpha_m(V) = \frac{0.07\exp(-0.1(V + 58)/20)}{\exp(-0.1(V + 58)/20) - 1}$ |
| | $\beta_m(V) = \frac{4e^{(-V + 60)/18}}{\exp(-V + 60)/18 + 1}$ |
| | $\beta_h(V) = \frac{1}{\exp(-0.1(V + 28) + 1)}$ |
| $I_K = g_Kn^4(V - E_K)$ | $\alpha_n(V) = \frac{-0.01(V + 34)}{\exp(-0.01(V + 34)/1) - 1}$ |
| | $\beta_n(V) = 0.125e^{(-V + 44)/80}$ |
Thus, the total derivative with respect to time of the above energy will be,

\[ \dot{H}(t) = CV \dot{V} + I_I E_I + I_{N_e} E_{N_e} + I_K E_K + I_M E_M + I_L E_Ca + I_T E_T. \]  

(3)

where \( E_I, E_{N_e}, E_K, \) and \( E_Ca \) are the Nernst potentials of leakage, the sodium, potassium and calcium ions in the resting state of the neuron. And \( I_I, I_{N_e}, I_K, I_M, I_L, \) and \( I_T \) are the ion currents of leakage, sodium, potassium, and calcium given by,

\[ I_I = g_I (V - E_I), \]

\[ I_{N_e} = g_{N_e} m^3 h (V - E_{N_e}), \]

\[ I_K = g_K n^4 (V - E_K), (I_K = \frac{g_K}{2} (1 - h)^4 (V - E_K)) \]

for TCR cell,

\[ I_M = g_M (V - E_K), \]

\[ I_L = g_L q^2 (V - E_Ca), \]

\[ I_T = g_T p^2 (V - E_T) \]

(4)

Substituting Equation (1) in (3), we have for the energy rate in the circuit,

\[ \dot{H}(t) = V I_{Stim} - I_I (V - E_I) - I_{N_e} (V - E_{N_e}) - I_K (V - E_K) - I_M (V - E_K) - I_L (V - E_Ca) - I_T (V - E_T). \]

(5)

Finally, replacing in Equation (5) the ion currents by their expressions given by Equation (4), the electrochemical energy rate in each neuron will be given by,

\[ \dot{H}_{cell} = V I_{Stim} - E_{cell}. \]

(6)

where cell=RS, FS, IB, TCR, RHI refers to the five conductance-based models considered in this work. This energy derivative provides the total derivative of the electrochemical energy in the neuron as a function of its state variables. The first term in the right hand summation represents the electrical power given to the neuron via the different junctions reaching the neuron and the \( E_{cell} \) represents the energy per second consumed by the ion channels (ion channels energy) involved in the dynamics.
of each cell model. The forms of the ion channels energies are given as:

\[
E_{RS} = g_l(V - E_l)^2 + g_{Na} m^3 h (V - E_{Na})^2 + g_K n^4 (V - E_K)^2 \\
+ g_{MP} (V - E_K)^2. \\
E_{FS} = g_l(V - E_l)^2 + g_{Na} m^3 h (V - E_{Na})^2 + g_K n^4 (V - E_K)^2, \\
E_{IB} = g_l(V - E_l)^2 + g_{Na} m^3 h (V - E_{Na})^2 + g_K n^4 (V - E_K)^2 \\
+ g_{MP} (V - E_K)^2 + g_l q^2 r (V - E_Ca)^2, \\
E_{TCR} = g_l(V - E_l)^2 + g_{Na} m^3 h (V - E_{Na})^2 \\
+ g_K (0.75(1 - h)(V - E_K)^2 + g_{MP}^2 \tau (V - E_T)^2, \\
E_{HFI} = g_l(V - E_l)^2 + g_{Na} m^3 h (V - E_{Na})^2 \\
+ g_K n^4 (V - E_K)^2. \\
\]

These equations permit evaluation of the total energy consumed by a given neuron and also give information about the consumption associated to each of the ion channels. Fundamentally, for each cell, this rate of energy expressed in nJ/s must be replenished by the ion pumps and metabolically supplied by hydrolysis of ATP molecules in order to maintain the cell’s spiking activity.

2.3. ION-COUNTING BASED ENERGY CONSUMPTION

The energy consumption can be also computed based on the amount of Na\(^+\) load (Q_{Na}) crossing the membrane during a single action potential, which it can be integrated estimating the area under the total Na\(^+\) current curve (see Figure 2) for the duration of stimulus presentation.

Since the Na\(^+\) gradient is maintained primarily by the activity of the Na\(^+\)/K\(^+\) ATPase which mediates influx of 2 K\(^+\) in exchange for 3 Na\(^+\) per one ATP molecule consumed, the number of ATP moles (ATPmol) can be computed as Q_{Na}/e, where e = 1.602 \times 10^{-19} \, C is the electric charge and NA = 6.022 \times 10^{23} is the Avogadro constant (Attwell and Laughlin, 2001). For the other hand, the energy available for chemical work from the ATP concentration is measured by the free energy of ATP hydrolysis (F_{ATP}). This allows an estimate of the metabolic energy associated with ionic pumping as the free energy times the number of ATP moles, that is, F_{ATP} \times ATPmol.

The value of the free energy depends to some extent on the internal chemical state of the cell, and it has been reported to be in the range from 46 to 62 kJ/mol of ATP (Janssen et al, 2003), but in this work, we set F_{ATP} = 50 kJ/mol.

Moreover, the integral of the area under the instantaneous energy function for a given cell (Equation 7) provides an estimate of the neuron energy, which is used to compute the efficiency of the ATP hydrolysis as the ratio of that energy consumption to the number of ATP moles, that is, \(\frac{1}{\text{ATPmol}} \int E_{cell}\). This ratio expressed is kJ/mol gives us the opportunity to check if our method of calculation of the actual energy consumption by the pump and the number of ATP molecules involved are consistent with other data in the literature. The calculated values of this ratio are reported in Figures 3, 6 as hydrolysis of ATP molecules.

3. RESULTS

3.1. FIRING CHARACTERISTICS OF ACTION POTENTIALS

The different possible combinations of conductances in the neuron models considered in this work give rise to a variety of action potentials with different waveforms and firing characteristics. Figure 1 reports, in part (A), trains of action potentials from different neuron models when exposed to prolonged stimuli of constant magnitude slightly greater than threshold (see Table 3 for a description of the current stimuli values). The inter-spike firing frequencies calculated from the inter-spike time intervals are reported in parts (B, C). As it can be seen, of all regular-spiking cells, the RS cell from ferret visual cortex (Cell 1) exhibits the most pronounced adaptation with an inter-spike firing frequency declining from about 62–3.5 Hz. Likewise, the IB cell as recorded respectively from guinea pig somatosensory cortex (Cell 6) and cat visual cortex (Cell 8), initially generate action potentials at high firing frequency (of about 55 Hz) that decrease rapidly to low values within a short time span. Meanwhile, the repetitive IB cell from guinea pig somatosensory cortex (Cell 7) shows repetitive intrinsic bursting with a mean inter-burst frequency of about 1 Hz, and an inter-spike frequency ranging from 300 to 150 Hz. The others cell models (i.e., Cells 4, 5, 9, and 10) respond to depolarizing stimuli by generating action potentials with little or no adaptation.

3.2. EFFICIENT ACTION POTENTIALS AND OVERLAPPING

Figure 2 shows in part (A) the shape of the sodium (in blue line) and potassium currents corresponding to a particular action potential of the previously described trains. The sodium current (in blue line) is negative but has been depicted with a positive sign for a better appreciation of the great extent of its overlapping with the potassium current (red line). Note that as sodium and potassium currents are both of positive charges but moving in opposite directions of the cell’s membrane they neutralize each other to the extent of their mutual overlap. The sodium charge that is not counterbalanced by simultaneously flowing potassium charge is much smaller for a greater overlap. This unbalanced load corresponds to the minimum charge (Q_{min}) needed for the depolarization of the action potential. The sum of this capacitive minimum and the overlap load gives the total Na\(^+\) loads per action potential. Recollected values are depicted in Figure 2B.

To quantify the sodium and potassium currents overlap we calculated the dimensionless charge separation as the ratio of the capacitive minimum and the total Na\(^+\) charge per action potential. That is, \(Q_{separation} = Q_{min}/Q_{Nat}\), this measure allows quantifying how efficiently sodium flux is used for action potential depolarization (Alle et al., 2009). In view of the above, it seems that rat hippocampal interneuron (Cell 10) and mouse thalamocortical relay neuron (Cell 9) are the most efficient in generating action potentials with a charge separation approaching 80%, which shows that most of sodium load are confined to the rising phase of the action potential. For the other hand, the FS cell from a ferret Visual Cortex (Cell 4) and the repetitive IB cell from a guinea pig somatosensory cortex in vitro (Cell 7) are the most inefficient with only 14% of sodium entry used for spike depolarization. In fact, the sodium influx during an action potential in thalamocortical relay neuron was 69 nC/cm², consuming
The values of stimuli (μA/cm²) are reported in Table 3. (B,C) The interspike firing frequencies calculated from the interspike intervals as a function of time.

0.24 pmol/cm² of ATP molecules per spike, while the FS cell from somatosensory cortex moves 217 nC/cm² of sodium ions per spike consuming 0.75 pmol/cm² of ATP molecules. Other models including RS cells from somatosensory cortex (Cell 2) and ferret visual cortex (Cell 1) show high values of Na⁺ loads of about 207 nC/cm² (0.72 ATP pmol/cm²) and 174 nC/cm² (0.60 ATP pmol/cm²), respectively. These estimates agree with other data reported in literature (Alle et al., 2009; Carter and Bean, 2009; Sengupta et al., 2010).

3.3. ENERGY
Assuming that one ATP molecule hydrolyzed under normal physiological conditions liberates of about 30 kJ/mol, our calculations of the energy demands in nJ per cm² based on the ion-counting method give energy consumptions ranging from 12 nJ/cm² for a thalamocortical relay cell (Cell 9) to 38 nJ/cm² for a FS cell from somatosensory cortex (Cell 5).

For the other hand, following the ion-channels energy functions described in Equation (7), the calculated values of the energy consumption give results which are in excellent agreement with those computed according to ion-counting approach. Indeed, according to the Wilcoxon rank-sum test (Gibbons and Chakraborti, 2011) performed on the data reported in Table 3, the difference between the values of metabolic and ionic energy is statistically not significant at the 5% significance level with a p-value = 0.8194.

The values of the energy consumption needed for the restoration of concentration gradients after an action potential was determined by integrating over long period of time the area under the instantaneous ion channels energy curve divided by the
Table 3 | Ionic flux and energy demands of single action potentials from different spiking cells when stimulated by prolonged current stimulus slightly greater than threshold.

|                  | RS cells | FS cells | IB cells | TCR | RHI |
|------------------|----------|----------|----------|-----|-----|
|                  | Cell 1   | Cell 2   | Cell 3   | Cell 4 | Cell 5 | Cell 6 | Cell 7 | Cell 8 | Cell 9 | Cell 10 |
| Frequency (Hz)   | 5        | 5        | 6        | 54   | 2     | 2      | 15     | 7     | 15     | 9       |
| Na\(^+\) load    | 174      | 207      | 134      | 162  | 217   | 132    | 103    | 147   | 69     | 163     |
| K\(^+\) load     | 141      | 214      | 150      | 156  | 197   | 137    | 117    | 133   | 79     | 127     |
| Capacitive minimum | 65      | 108      | 70       | 22   | 129   | 37     | 15     | 51    | 55     | 125      |
| Overlap load (nC/cm²) | 109   | 99       | 64       | 140  | 88    | 95     | 88     | 96    | 14     | 38       |
| Charge separation | 0.38     | 0.52     | 0.52     | 0.14 | 0.60  | 0.28   | 0.14   | 0.35  | 0.79   | 0.77     |
| ATP Pmole        | 30       | 36       | 23       | 28   | 38    | 23     | 18     | 25    | 12     | 28       |
| Metabolic Energy (nJ/cm²) | 30     | 34       | 20       | 24   | 38    | 23     | 18     | 30    | 12     | 23       |
| Ionic Energy (From Equation 7) (nJ/cm²) | 49.14 | 47.03    | 43.93    | 41.96 | 51.15 | 49.70 | 51.91 | 59.95 | 48.78 | 40.82   |
| ATP Hydrolysis (kJ/mol) | 1.4    | 0.7      | 0.15     | 1.75 | 0.8   | 0.25   | 0.25   | 2.25  | 0.44   | 0.20   |

The metabolic energy refers to the energy computed according to the ion-counting approach (section 2.3), and the ionic energy accounts for the electrochemical energy computed as the integral of the energy functions given by Equation (7).

The number of spikes, which gives the energy consumption of a single spike. In Figure 3 we report the free energy of ATP hydrolysis computed as the ratio of the ionic energy and the number of ATP molecules. This ratio is expressed in kJ/mol and gives values ranging from 40.82 kJ/mol in the case of a rat hippocampal interneuron (Cell 10) and value of about 60 kJ/mol for an IB cells as observed from cat visual cortex (Cell 8). These values are in nice agreement with the values of the free energy of ATP hydrolysis reported in the literature (Ereciriska et al, 1989; Jansen et al, 2003).

3.4. TEMPERATURE AND STIMULUS INTENSITY

Because neural properties are temperature dependent, we have analyzed in more detail the values of energy consumption and the free energy of ATP hydrolysis as a function of temperature and the magnitude of the external stimuli. Varying the cell temperature in
the neuron models was down multiplying the rates of change of the activation and inactivation gating variables by a factor $k = 2.78^{(\text{Temp} - 36)/10}$, and considering a range of temperature between 20°C and 40°C. The stimuli were varied from 2.25 to 10 $\mu$A/cm².

The contour plots in Figure 5 show, for each cell, how the energy consumption in nJ/cm² per spike depends upon cell temperature and input stimulus. As it can be seen the lowest energy consumption values are achieved for higher temperatures. In fact, the increased firing frequencies induced by higher temperatures and stimulus (see Figure 4) imply more efficient use of sodium entry due mainly to the reduced overlap load between inward Na⁺ current and outward K⁺ current (Moujahid et al., 2012). Indeed, for all cells, the overlap load undergoes a reduction of about 90% with an increase of cell temperature in a wide range of stimulus intensity. This efficient use of sodium entry is usually accompanied by a reduction of the energy demands needed for the restoration of concentration gradients. For example, the rat hippocampal interneuron (Cell 10) at 20°C and an input stimulus of 2.25 $\mu$A/cm² fires spikes at 55 Hz and consumes of about 58 nJ/cm². While at a higher temperature of about 40°C for a wide range of stimulus intensity, the energy consumption is about 5-fold lower that the energy needed at low temperatures. This 5-fold decrease in energy consumption corresponds to 7-fold increase in firing frequency for an input stimulus of 10 $\mu$A/cm². Likewise, the IB cell as observed from cat visual cortex (Cell 8) consumes of about 109 nJ/cm² at 20°C and lower stimulus, however, at 40°C it requires only 13 nJ/cm² which represents of about 8-fold decrease in its energy demand. At this temperature the values of energy consumption are maintained for a wide range of input stimulus.

3.5. THE FREE ENERGY OF ATP HYDROLYSIS

Figure 6 shows the calculated values of ATP hydrolysis in kJ/mol as a function of temperature and stimulus intensity. In this case, we observe different patterns depending on the cells type. The RS and FS cells at higher temperatures and high input stimuli liberate, respectively of about 12% and 10% more free energy than at lower temperatures. For these cells the values of free energy liberated range from 40.73 kJ/mol in the case of FS cell from a ferret Visual Cortex (Cell 4) to 47.74 kJ/mol in an inhibitory RS cell from somatosensory cortex in vitro (Cell 3). The IB cells in guinea pig somatosensory cortex (Cells 6 and 7) show similar pattern as observed in regular and fast spiking cells, but in this case, increasing the cell temperature and stimulus intensity cause the free energy to experience an increase of more than 17% reaching values of about 52.27 kJ/mol. But, the more sensible cells to temperature and stimulus changes are IB cells as observed from cat visual cortex (Cell 8) and mouse thalamocortical relay neuron (Cell 9). Cell 8 shows values of free energy that range from 44.58 kJ/mol to 61.21 kJ/mol representing an increase of about 37%. For this cell, the higher values of free energy are achieved for higher temperatures and low values of stimulus. In fact, the more pronounced pattern was observed for values of stimulus below 3 $\mu$A/cm², and a further increase of stimulus has seems to have little effect on free energy values. Conversely, Cell 9 accounting for a mouse thalamocortical relay neuron appears to be more sensitive to stimulus intensity than to temperature values. Increasing stimulus intensity from 2.25 to 10 $\mu$A/cm² moves the cell to liberate of about 22% more free energy of ATP hydrolysis. Finally, for Cell 10 corresponding to a rat hippocampal interneuron, we can see that for values of input stimulus below 8 $\mu$A/cm², the free energy shows an hyperbole surface with a maximum around 33°C.

4. DISCUSSIONS

Based on three computational neuron models (see Table 1), we used different combinations of voltage-dependent conductances to reproduce a variety of action potentials with different waveforms and firing characteristics as recorded from different cells in the neocortex, thalamus and hippocampus. Initially, each cell was stimulated by prolonged depolarizing stimulus slightly greater than threshold. We calculated in nC/cm² the amount of Na⁺ load crossing the membrane during a single action potential.
FIGURE 4 | The firing frequency (Hz) as a function of the cells temperature and the external depolarizing stimulus. We consider a range of temperature between 20°C and 40°C, and a stimulus varying from 2.25 to 10 μA/cm².

and the corresponding metabolic energy nJ/cm² needed for the restoration of concentration gradients after an action potential following two different approaches (see section 2). According to our calculations, for all the cells considered in this work, these two approaches have led to similar values of energy demands which confirms the consistency of our method to estimate the metabolic consumption. In fact, the range of values of our estimations of the free energy of ATP hydrolysis (see Figures 3, 6) agree with other data reported in the literature (Ereciriska et al, 1989; Jansen et al, 2003).
An initial classification of the different cells (see Table 3, Figure 3) places the thalamocortical relay cell (Cell 9) as the most energy-efficient cell consuming 12 nJ/cm² for each spike generated and liberating a free energy of ATP hydrolysis of about 48.78 kJ/mol. For the other hand, the FS cell from somatosensory cortex (Cell 5) is the least energy-efficient requiring 38 nJ/cm² per spike and liberating 51.15 kJ/mol of free energy from ATP hydrolysis.
To quantify how the energy consumption in nJ/cm² and then the free energy of ATP hydrolysis depend upon cell temperature and input stimulus, we analyzed in more detail the values of these measures for a wide range of cell temperatures and stimulus intensities. The results give a clear evidence that the metabolic energy associated to the generation of action potentials is higher at lower temperature. Indeed, the spiking activity of the cells at higher temperatures involves less ion flux during the generation of an action potential. In all the neurons studied in this work, increasing the cell temperature from 20°C to 40°C resulted in
decreases by about 80% in both the sodium and potassium flux. Obviously, this decrease in ion flux should be accompanied by a decrease in energy consumption. In fact, results reported in Figure 5 support this conjecture showing that low values of energy are achieved at higher temperatures. For a given temperature and stimulus intensity, for example, at 36°C and a stimulus value of 7 μA/cm², the energy consumptions range from 8.42 nJ/cm² in the case of cell 9 to 26.8 nJ/cm² in the case of cell 5 and 28.5 nJ/cm² in cell 2. The other cells show value of studying population of coupled neurons.

Our approach to find an energy function that quantifies the physical and information processing of large population of interconnected neurons. For this end, we need to combine experimental studies of nervous systems with numerical simulation of large-scale brain models. Our approach to find an energy function that quantifies the physical energy associated to the states of a generic model neuron described by differential equations could be of great interest when studying population of coupled neurons.

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