Spin excitations in nickelate superconductors

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Applying a three-band model and the random phase approximation, we theoretically study the spin excitations in nickelate superconductors, which have been newly discovered. The spin excitations were found to be incommensurate in the low energy region. The spin resonance phenomenon emerged as the excitation energy increased. The intensity can be maximized at the incommensurate or commensurate momentum, depending on the out-of-plane momentum. The spin excitations reverted to incommensurate at higher energies. We also discuss the similarities and differences in the spin excitations of nickelate and cuprate superconductors. Our predicted results can be later validated in inelastic neutron scattering experiments.

nickelates, superconductivity, d-wave pairing, spin susceptibility

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1 Introduction

High-$T_c$ cuprate superconductivity was discovered over thirty years ago, but understanding its microscopic mechanism has been a challenging task [1]. Undoubtedly, exploring cuprate analogs has revealed a new family of superconductors and has enhanced our understanding of cuprate superconductor physics [2-4]. The Ni atom is close to the Cu atom on the periodic table. Early efforts realized infinite-layer $RNiO_2$ ($R=La$, Nd) compounds [5-7], which are isostructural to CaCuO$_2$ [8], a parent compound of cuprate superconductors. The Ni$^{2+}$ in $RNiO_2$ has a 3d$^9$ configuration, similar to the Cu$^{2+}$ in high-$T_c$ cuprate superconductors. Therefore, the nickelates are strong potential candidates of cuprate analogs, and have attracted considerable attention for this reason [5-7, 9-14]. However, nickelates differ from cuprates in two respects: $RNiO_2$ may be metallic rather than a magnetic insulator [6, 7, 10-14], and the Ni-d$_{x^2-y^2}$ band in LaNiO$_2$ may mix with the La-5d band at low energies [12, 13].

Very recently, superconductivity with $T_c$ in the 9-15 K range was discovered in the Sr doped infinite-layer nickelate material Nd$_{1-x}$Sr$_x$NiO$_2$ [15]. This new discovery has reinvigorated studies in the electronic structure and physical properties of nickelates [16-37]. Of crucial importance is reconsidering the differences and similarities between nickelates and cuprates, and identifying the superconductivity mechanism of nickelates. Some experiments have yielded contrary results, namely, no superconductivity has been observed in bulk sample [30] or film samples of Nd$_{1-x}$Sr$_x$NiO$_2$ [32]. Based on density functional theory, Si et al. [33] concluded that 3d$^9$-
type $R$NiO$_2$ is analogous to the cuprates despite these negative findings. In some nickelate samples, superconductivity is lost through hydrogen intersection, which favors the 3d$^9$ configuration of nickel ions.

Although the mechanism of high-$T_c$ superconductivity remains puzzling, spin excitations are thought to play an important role. Accordingly, the spin excitations in cuprate superconductors have been intensively studied, both experimentally [38-43] and theoretically [44-56]. The momentum and frequency dependences of spin excitations have been experimentally studied in inelastic neutron scattering (INS) experiments. Meanwhile, theoretical studies of spin excitations have explored the imaginary part of the dynamical spin susceptibility. The theoretical results qualitatively concur with the experimental observations. In the superconducting state, the resonant spin excitation at the commensurate momentum $(\pi, \pi)$ occurs at a certain resonant energy. Below and above the resonant energy, the intensity of the spin excitation decreases rapidly and the momentum moves to an incommensurate state [38-56]. This is among the most important results of superconductivity. The parent compounds $R$NiO$_2$ of nickelates are metallic and lack magnetic order [6, 7, 10-15]. At first glance, the nickelates appear with later INS experimental results would unambiguously reveal whether nickelates are cuprate-like superconductors, and would help to elucidate the mechanism of nickelate superconductivity.

Several models of nickelate band structure have been proposed in recent years. These models include the single-band [16, 19, 27], two-band [18, 21, 26], three-band [19, 20], and higher multi-band models [17]. In general, spin excitations are determined by the geometry of the Fermi surface [47-49, 51, 54]. We first consider the d-wave superconducting pairing in a three-band model. To investigate the spin excitations, we apply random phase approximation (RPA). Our numerical results suggest the presence of quasi-spin-resonance at a typical resonant energy. At low and very high energies, the spin excitations are generally incommensurate, which can be well understood in terms of Fermi surface scattering. The similarities and differences between the spin excitations of nickelates and cuprates are then discussed.

The remainder of the paper is organized as follows. Sect. 2 introduces and formulates the model. Sect. 3 reports the numerical calculations and discusses the obtained results. The paper concludes with a brief summary in sect. 4.

## 2 Model and formalism

We start from the Hamiltonian including the hopping term, the superconducting pairing term, and the interaction term, expressed as:

$$ H = H_1 + H_p + H_{\text{int}}. $$

(1)

The hopping term $H_1$ is obtained from a three-band tight-binding fit from the first-principal band structure of the Nd$_{0.8}$Sr$_{0.2}$NiO$_2$ compound [19],

$$ H_1 = - \sum_{i j k} t_{i j k}^\sigma c_{i \sigma}^\dagger c_{j \sigma} + \mu_0 \sum_{i j} c_{i \sigma}^\dagger c_{i \sigma}. $$

(2)

Here $c_{i \sigma}$ ($c_{i \sigma}^\dagger$) are creation (annihilation) operators at the $i$th site in the orbital $\sigma$ and with spin projection $\sigma$. The indices $i$ and $\sigma$ run through 1 to 3 corresponding to the Ni-3d$_{x^2-y^2}$ orbital, the Nd-5d$_{3z^2-r^2}$ orbital, and the Nd-5d$_{xy}$ orbital, respectively.

$H_p$ is the superconducting pairing term, expressed as:

$$ H_p = \sum_{i j} (\Delta_{i j} c_{i 1 \uparrow}^\dagger c_{j 1 \uparrow}^\dagger + \text{h.c.}). $$

(3)

Following ref. [19] and assuming that the electron pairing is mediated by the spin excitations, only the electron pairing within the Ni-3d$_{x^2-y^2}$ orbital is considered.

The electron interaction term $H_{\text{int}}$ is expressed as:

$$ H_{\text{int}} = \sum_{i \alpha \sigma \alpha'} U_{\alpha \sigma \alpha'} n_{i \alpha \sigma} n_{i \alpha' \sigma'} + J_H \sum_{i \alpha \sigma} (c_{i 2 \alpha}^\dagger c_{i 1 \alpha'}^\dagger c_{i 2 \alpha} c_{i 1 \alpha'} + \text{h.c.})

+ J' \sum_{i} (e_{i 2 1}^\dagger e_{i 2 1}^\dagger e_{i 3 1} c_{i 3 1} + \text{h.c.}), $$

(4)

where $U_{\alpha \sigma}$ and $U_{\alpha' \sigma}$ ($\alpha \neq \alpha'$) represent the intra-orbital and inter-orbital interactions, respectively. $J_H$ and $J'$ are the Hund’s coupling constant and the pairing hopping constant of the two Nd-5d orbitals.

Defining a six order column vector with $\Psi(k) = (c_{i 1 \uparrow}, c_{i 2 \uparrow}, c_{i 3 \uparrow}, c_{i 1 \downarrow}, c_{i 2 \downarrow}, c_{i 3 \downarrow})^T$, the above bare Hamiltonian without the interaction term can be expressed as the $6 \times 6$
matrix term in the momentum space. The bare spin susceptibility including both the normal and the anomalous terms is then expressed as:

\[ \chi_{\alpha}^{\alpha'}(q, \omega) = \frac{1}{N} \sum_{kij} \left[ u_{\alpha i}(k) u_{\alpha' j}(k + q + k) + u_{\alpha j}(k + q) u_{\alpha' j}(k + q + k) \right] \times \frac{f(E_i(k + q)) - f(E_i(k))}{\omega - E_i(k + q) + E_i(k) + i\delta}, \]

(5)

where \( u_{\alpha i}(k) \) and \( E_i(k) \) are eigenvectors and eigenvalues of the Hamiltonian which can be obtained through diagonalizing the Hamiltonian matrix. The cases with \( \alpha = \alpha' \) and \( \alpha \neq \alpha' \) are corresponding to the intra-orbital excitations and inter-orbital excitations, respectively. Generally both the inter-orbital scattering and the intra-orbital scattering may contribute to the spin susceptibility. While from the present band structure, the three orbitals are weakly coupled and the spin susceptibilities from the inter-orbital scattering are nearly vanishing. As a result, only intra-orbital spin excitations related to intra-orbital interaction terms in eq. (4) need to be considered. Moreover, the renormalized spin susceptibilities contributed by the Nd-layer are negligibly small in the whole momentum and energy space we considered. More details and the numerical verifications have been presented in Supporting Information. Then, following refs. [55,56], here only the scattering within the Ni-3d \( t_{2g} \) orbital is considered with \( \chi_0(q, \omega) = \chi_{0}^{11}(q, \omega) \).

The renormalized spin susceptibility can be obtained through the RPA [44,46], which is given by

\[ \chi(q, \omega) = \frac{\chi_0(q, \omega)}{1 - U \chi_0(q, \omega)}, \]

(6)

where \( U = U_{11} \) is the on-site Hubbard-like interaction in the Ni-3d \( t_{2g} \) band.

In the following presented results, we use the nearest-neighbor hopping constant of the Ni-3d band as the energy unit. Other in-plane hopping constants are taken from ref. [19] and presented in Supporting Information.

3 Results and discussion

We now study the spin excitations in the normal state by setting the gap magnitude \( \Delta_0 = 0 \) in eq. (1). At first we shall justify the effective on-site interaction \( U \) in the RPA factor. In the RPA theory, the effective interaction \( U \) differs from the original on-site repulsive interaction. Usually the former is much smaller than the latter to ensure the RPA framework to be correct [44,46]. Also, for the \( t-J \) model type, it was proposed that the renormalized interaction in the RPA theory should multiply an additional factor \( \alpha = 0.34 \) to match the antiferromagnetic instability [51]. Therefore, it is difficult to determine \( U \) directly from the band calculation. While one can obtain an effective range for the value of \( U \) from the magnetic instability. In the framework of RPA, the magnetic instability occurs when the pole condition of the real part of the zero energy RPA factor occurs \((1 - U \text{Re} \chi_0(q, 0) = 0)\).

We plot the real part of the zero energy normal state bare spin susceptibility as a function of the in-plane momentum \( q \) in Figure 1(a). As is seen, the maximum value of \( \text{Re} \chi_0(q, 0) \) is about 0.346. To avoid the magnetic instability, the effective \( U \) should be taken as \( U < 2.89 \). Note that the doping density is 0.2, which is far away from the antiferromagnetic instability point. In the following presented results, we choose \( U = 2 \). We have checked numerically that the results are stable when the value of \( U \) changes slightly.

The imaginary parts of the spin susceptibility as a function of the in-plane momentum \( q \) with the energy \( \omega = 0.1 \) are plotted in Figure 1(b). As is seen, the main contributions of the spin excitations are around the antiferromagnetic momentum \((\pi, \pi)\). The maximum spin excitations occur at an incommensurate in-plane momentum \( q_1 \), with \( q_1 \approx (0.55\pi, \pi) \). The maximum intensity increases as the out-of-plane momentum \( q_z \) increases. The momentum \( q_0 \) depends weakly on \( q_z \).

The intensity plots of the imaginary parts of the spin susceptibilities as functions of the momentum and the energy in the normal state with different \( q_z \) are plotted in Figure 2(a)-(c). For the case of \( q_z = 0 \), the main spin excitations are around the incommensurate in-plane momentums \((\pi \pm \delta, \pi)\).

![Figure 1](https://example.com/figure1.png)

Figure 1 (Color online) (a) The real parts of the bare normal state spin susceptibility as a function of the momentum \( q \) with \( \omega = 0 \). (b) The imaginary parts of the renormalized normal state spin susceptibility as a function of the momentum \( q \) with \( \omega = 0.1 \).
tries. For the case of the present work, there are three possible pairing symmetries: the electron pairings within the NiO$_2$ layer nearest-neighbor hopping constants. Therefore, only is the isotropic s-wave pairing with $\Delta$ for the Ni-3d tent with the tight-binding band parameters from the band to the existence of the Nd-layers, the coupling between different NiO$_2$ planes. Due to the existence of the Nd-layers, the coupling between different NiO$_2$ layers should be weak. This is also consistent with the tight-binding band parameters from the band calculation $^1$, namely, the inter-layer hopping constants for the Ni-3d orbital are much smaller than the intra-layer nearest-neighbor hopping constants. Therefore, only the electron pairings within the NiO$_2$ plane are considered in the present work. There are three possible pairing symmetries. For the case of $j = i$ in eq. (3), the pairing symmetry is the isotropic s-wave pairing with $\Delta = \Delta_0$. When $j$ is the nearest-neighbor site to $i$, the pairing symmetry may be the extended s-wave pairing state with $\Delta_{ij} = \Delta_0/4$, or the d$_x^2$-y$^2$ pairing state with $\Delta_{ij} = \pm \Delta_0/4$ ($\pm$ depend on the bond $(ij)$ being along the x direction or the y direction). In the momentum space, through Fourier transformation, these two pairing symmetries are expressed as $\Delta_k = \Delta_0(\cos k_x + \cos k_y)/2$ and $\Delta_k = \Delta_0(\cos k_x - \cos k_y)/2$, respectively.

The most possible pairing symmetry can be further investigated from the above normal state spin excitations presented in Figure 1, namely, the NiO$_2$ planes are hole-doped from the half-filled Mott insulators. There may exist significant spin excitations near the antiferromagnetic in-plane momentum ($\pi$, $\pi$), which may in principle generate in-plane superconducting d-wave pairing. Previously based on the spin fluctuation scenario, the d$_x^2$-y$^2$ pairing symmetry is indeed supported $^{17,19}$. In the following, we follow refs. $^{17,19}$ and consider the pairing symmetry as the d-wave pairing within the NiO$_2$ plane. For the infinite-layer phase, each NiO$_2$ plane is equivalent. Therefore, the gap magnitude $\Delta_0 = 0.2$ is considered below, independent on the z-axis coordinates.

Now let us study the energy dependence of the spin excitations. One of most important results in the superconducting state is the resonant spin excitations. The possible spin resonance has been studied theoretically in many unconventional superconducting systems, including the cuprates $^{50-56}$, the iron-based superconductors $^{57-61}$, the Na$_2$CoO$_2$.yH$_2$O superconductors $^{62}$, and the heavy fermion material CeCoIn$_5$ $^{63}$. Here we would like to explore whether the spin resonance exists in nickelate superconductors. The imaginary parts of the spin susceptibilities as a function of the energy at the in-plane momentum $Q_{0y} = (\pi, \pi)$ are displayed in Figure 3. For comparison, we also present the spin susceptibilities in the normal state, the isotropic s-wave pairing state and the extended s-wave pairing state in Figure 3. Then it is seen clearly that a spin resonance peak occurs near the energy 0.4 (about twice of the gap magnitude) for the spin excitation in the d-wave superconducting state. For the isotropic s-wave pairing state, the spin excitations are nearly vanishing within the superconducting gap and no spin resonance occurs. For the extended s-wave pairing state, no gap feature is seen. The spin excitation is almost the same as that of the normal state and no spin resonance exits, either. This can be explained well through exploring the nodal lines of the extended s-wave pairing. They coincide with the boundaries of the magnetic Brillouin zone, expressed as $(k_x = \pi \pm k_y)$. The spin excitations at the momentum ($\pi$, $\pi$) are mainly contributed by the scattering between boundaries of the magnetic Brillouin zone. Thus the superconducting pairing has no effect on the ($\pi$, $\pi$) spin excitation for this extended s-wave pairing symmetry.

The energy dependence of the spin excitations may be studied by later INS experiments. The existence of the spin resonance at the in-plane momentum ($\pi$, $\pi$) may be tested and taken as one important signature for the d-wave superconductivity. The spin resonance is robust for different $q_z$. The position changes slightly as $q_z$ changes.
The intensity plots of the imaginary part of the spin susceptibility as a function of the energy for different energies and different in-plane momenta are presented in Figure 4. For the case of $q_z = 0$, when the energy is below the resonant energy, as is seen in Figure 4(a), four incommensurate peaks at the momentums $(\pi \pm \delta, \pi)$ and $(\pi, \pi \pm \delta)$ are seen clearly. As the energy increases to the resonant energy, as is seen in Figure 4(b), the spin excitation at the momentum $(\pi, \pi)$ increases greatly, while the spin excitation is still incommensurate at this energy and the incommensurability is rather small. When the energy increases further to above the resonant energy (Figure 4(c)), the spin excitation is still incommensurate while the incommensurability is large. The numerical results for $q_z = 0.5\pi$ are displayed in Figure 4(d)-(f). At low energy with $\omega = 0.2$, the spin excitation is also incommensurate. The maximum spin excitations form a circle around $(\pi, \pi)$. Near the resonant energy, the maximum spin excitation still occurs at an incommensurate momentum and the incommensurability is still rather large. Above the resonant energy with $\omega = 0.8$, the spin excitation is also incommensurate. When the out-of-plane momentum $q_z$ increases to $\pi$, as is seen in Figure 4(g)-(i), the spin excitations are incommensurate at low and high energies. Near the resonant energy, the spin excitation is commensurate.

To study the energy dependence of the spin excitations more clearly, the intensity plots of the imaginary part of the spin susceptibility as functions of the momentum and energy are presented in Figure 5. The incommensurability reaches the minimum at the energy about 0.4. For higher energies ($\omega > 0.6$), the superconducting order parameter plays a relatively minor role and the dispersion at this energy region is similar to those of the normal state (presented in Figure 2). As $q_z$ increases to 0.5, the spin excitation is commensurate near the energy 0.6. While at the energy 0.4, where the spin resonance is excepted, the spin excitation is still incommensurate. Actually, the spin excitations at this momentum are similar to those in La-based cuprate superconductors [54, 64]. As discussed in ref. [54], when the spin resonance is weak, the incommensurate spin excitation may occur. The commensurate spin excitation at higher energies is consistent with the bare spin susceptibility. For the case of $q_z = \pi$, as is seen, the dispersion is downward at low energies and upward at high energies. The spin excitation is commensurate near the resonant energy. For all of $q_z$ we considered, a hourglass dispersion is seen clearly. Note that, the dispersion may also be obtained from INS experiments. For cuprate superconductors, the hourglass dispersion has also been reported both experimentally and theoretically [42, 43, 51, 54]. Actually, the dispersion of the maximum spin excitations is closely related to the band structure, the Fermi surface, and the pairing symmetry of the material. We expect that our theoretical predic-
spin susceptibility as a function of the in-plane momentum ($q_x$) and the energy in the superconducting state with different out-of-plane momenta $q_z$. (a) $q_z = 0$; (b) $q_z = 0.5\pi$; (c) $q_z = \pi$.

Figure 5 (Color online) The intensity plots of the imaginary part of the spin susceptibility as a function of the out-of-plane momentum ($q_z$) and the energy in the superconducting state with different in-plane momenta ($q_x$). (a) $q_x = 0$; (b) $q_x = 0.5\pi$; (c) $q_x = \pi$.

Figure 6 (Color online) (a) The normal state Fermi surfaces. The solid arrow indicates the intra-orbital scattering with $Q_1 = (\pi, \pi)$. The two dashed arrows indicate the inter-orbital scattering with $Q_2 = (0.6\pi, 0.6\pi)$ and $Q_3 = (0.4\pi, 0.4\pi)$. (b) The constant energy contours. (c) The real part of the RPA factor and the imaginary part of the bare spin susceptibility as a function of the energy.
also provide a potential justification of the models if such co-existence is detected by experiments.

For the case of low energy spin susceptibility in the superconducting state, only excitations near nodes can occur. Thus qualitatively speaking, the low energy spin excitations are qualitatively similar for different $q_z$. A more insightful explanation for the low energy incommensurate spin excitations can be obtained through the constant energy contours. According to ref. [51], at low energies, the spin excitations are mainly determined by the bare spin susceptibilities. Generally, the scattering between the energy contours $E_k = \omega_j/2$ is responsible for the spin excitations at the energy $\omega_j$. The contour plots of the quasiparticle energy with $E_k = 0.1$ for different $k_z$ are plotted in Figure 6(b). As is seen, for all of $k_z$, we considered, the contours for different $k_z$ are qualitatively similar. Therefore, the spin excitations at the energy $\omega = 0.2$ are qualitatively similar and are incommensurate for different out-of-momentum $q_z$.

We depict the real part of the RPA factor $\text{Re}A(Q, \omega) \ (\Lambda = 1 - U_\chi)$ and the imaginary part of the bare spin susceptibility $\text{Im} \chi_0$ in Figure 6(c) to look into the mechanism of the spin resonance. Here the spin resonance arises from the RPA renormalized effect. Firstly let us summarize the mechanism for the spin resonance in cuprate superconductors [51,52]. At low energies, the energy contours do not touch the hot spot (the crossing points of Fermi surface with the magnetic Brillouin zone boundary). Therefore, $\text{Im} \chi_0$ tends to zero at the in-plane momentum $(\pi, \pi)$, i.e., a spin gap exists. The spin gap closes when the constant energy contour reaches the hot spot. Usually for hole-doped cuprate compounds, the hotspot is near the momentum $(\pi, 0)$. Thus the spin gap is about $2\Delta_0$ ($\Delta_0$ is the gap magnitude at the momentum $(\pi, 0)$). Due to the flat band at this momentum (extended van Hove singularity), a step-like rise of $\text{Im} \chi_0$ occurs at the edge of the spin-gap. Then a logarithmic singularity in $\text{Re} \chi_0$ occurs via the Kramers-Kronig relation. This singularity will lead to the pole condition of the RPA factor being satisfied within the spin-gap. As a result, a sharp resonance peak appears for the imaginary part of the RPA factor $\text{Im} \chi_0$ in Figure 6(c) to look into the mechanism of the spin resonance. Here the spin excitation is enhanced greatly for a typical d-wave superconducting state. As the pole condition is not really satisfied, the RPA renormalized effect is not as strong as that in cuprates. Therefore, for some $q_z$, the spin excitation may still be incommensurate even at the resonant energy.

As the energy increases further, the RPA renormalization has a rather weak effect. Then the spin excitations are still determined by the bare spin susceptibility, similar to the case of low energy excitations. While at the high energy, the antinodal to antinodal excitations play an important role. The normal state Fermi surface splits at the antinodal direction for different $k_z$. Thus the spin excitations for $q_z = 0$ and $q_z = 0$ are different. For the case of $q_z = 0$, only the scattering between the same Fermi surface occurs. For the case of $q_z = 0$, the spin excitations are determined by scattering between the Fermi surface with different $k_z$. Then the weak disorder is induced. It is noted that the spin excitations along different directions are almost the same as those shown in Figure 4.

Let us summarize the similarities and differences of the spin excitations in the d-wave superconducting state between the cuprates and nickelates. Firstly, although the band structure of nickelates is three dimensional, the properties of the spin excitations are qualitatively similar for different $q_z$. The maximum spin excitations are always around the momentum $(\pi, \pi)$, which is indeed similar to those of cuprates. Secondly, in both compounds, a spin resonance phenomena can be observed, namely, the spin excitation is enhanced greatly in the superconducting state at the energy about $2\Delta_0$. The third similarity is that the spin excitations are incommensurate at low and high energies. Especially, the low energy spin excitations are nearly identical to those of cuprates. On the other hand, there still exist some differences for the spin excitations of these two families. In nickelates, the spin resonance is damped greatly. Therefore for some $q_z$, the maximum excitation does not occur at the momentum $(\pi, \pi)$. Moreover, the incommensurate spin excitations depend on the out-of-plane momentum $q_z$. The maximum points may form a circle at the momentum space for certain $q_z$. These similarities and differences may be detected by later INS experiments.

At last, we would also like to discuss the difference of spin excitations between nickelates and iron-based superconductors. In iron-based superconductors, as discussed in ref. [57], the d-orbitals from iron ions are heavily entangled thus rather strong hybridization exists. Moreover, each Fermi pocket is contributed by several orbitals. Therefore, the inter-pocket scattering is important to determine their spin excitations [57-61]. For nickelates, although a three-orbital model is taken to generate three Fermi surface pockets, while from the present band structure we considered, each Fermi pocket is mainly contributed by one orbital and the inter-pocket coupling is weak. As have discussed, the spin excitations are mainly contributed by the Ni-3d$_{x^2-y^2}$ band. The other two
Nd-5d orbitals play a minor role. Also, based on our present model the spin excitations from the inter-pocket scattering are also rather small.

4 Summary

In summary, starting from a three-band model and d-wave superconductivity, we have examined the spin excitations in the nickelate superconductors based on the random phase approximation. A spin resonance phenomenon, namely, the spin excitation is enhanced in the superconducting state at the energy about twice of the gap magnitude, was revealed. Below and above the resonant energy, the spin excitations are incommensurate. The similarities and differences for the spin excitations in the nickelates and cuprates have been discussed. All of the numerical results are explained well based on the geometry of Fermi surface.

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Supporting Information

The supporting information is available online at phys.scichina.com and link.springer.com. The supporting materials are published as submitted, without typesetting or editing. The responsibility for scientific accuracy and content remains entirely with the authors.

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