Ionospheric GNSS Imagery of Seismic Source: Possibilities, Difficulties, and Challenges

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Abstract

Up to now, the possibility to obtain images of seismic source from ionospheric Global Navigation Satellite Systems (GNSS) measurements (seismo-ionospheric imagery) has only been demonstrated for giant earthquakes with moment magnitude \(M_w \geq 9.0\). In this work, we discuss difficulties and restrictions of this method, and we apply for the first time the seismo-ionospheric imagery for smaller earthquakes. The latter is done on the example of the \(M_w 7.4\) Sanriku-oki earthquake of 9 March 2011. Analysis of 1-Hz data of total electron content (TEC) shows that the first coseismic ionospheric disturbances (CID) occur \(\approx 470-480 \) s after the earthquake as TEC enhancement on the east-northeast from the epicenter. The location of these first CID arrivals corresponds to the location of the coseismic uplift that is known as the source of tsunamis. Our results confirm that despite several difficulties and limitations, high-rate ionospheric GNSS data can be used for determining the seismic source parameters for both giant and smaller/moderate earthquakes. In addition to these seismo-ionospheric applications, we raise several fundamental questions on CID nature and evolution, namely, one of the most challenging queries—can moderate earthquake generate shock-acoustic waves?

Plain Language Summary

Ionosphere is a layer of charged particles of the Earth’s atmosphere located at altitudes \(\approx 60–800 \) km. However, despite being high above the Earth’s surface, the ionosphere is sensible to numerous near-ground geophysical events (earthquakes, tsunamis, volcano eruptions, etc). Acoustic and gravity waves emitted by these events propagate upward and generate atmospheric/ionospheric perturbations. Ionospheric disturbances generated by earthquakes are known as coseismic ionospheric disturbances (CID). Recently, it has been suggested that analysis of CID and their first arrivals can provide information on the position and on the structure of seismic fault ruptured in earthquake. This method is known as ionospheric imagery of seismic source. However, so far, this method has been only applied to giant earthquakes (\(M_w \geq 9.0\)). In this work, for the first time, we apply the ionospheric imagery for smaller earthquakes on the example of the \(M_7.4\) Sanriku-oki earthquake that occurred on 9 March 2011 in Japan. Our results show that this method is applicable to smaller earthquakes, and despite some difficulties, it can indicate the position of coseismic uplift \(\approx 8 \) min after the earthquake. The uplift generates CID but also tsunamis. Therefore, our method can be used as independent or complementary one for near–real-time tsunami warning systems.

1. Introduction

It is now well demonstrated that earthquakes can generate perturbations in the ionosphere (e.g., Afraimovich et al., 2001, 2010; Astafyeva & Heki, 2009; Bagiya et al., 2018; Calais & Minster, 1995; Heki & Ping, 2005; Jakowski et al., 2006; Komjathy et al., 2016; Liu et al., 2011; Perevalova et al., 2014; Rolland et al., 2011; Zettergren & Snively, 2015). During an earthquake, a sudden impulsive forcing from the ground or ocean floor generates atmospheric pressure waves that propagate upward into the ionosphere. These perturbations are called co-seismic ionospheric disturbances (CID). Spatio-temporal and dynamic features of CID have been extensively investigated within the last decade by using signals of Global Navigation Satellite Systems (GNSS; e.g., Astafyeva et al., 2009, 2014; Bagiya et al., 2017; Ducic et al., 2003; Jin et al., 2010; Rolland et al., 2011, 2013).

Apart from systematic detection of earthquakes in the ionosphere, more recently, it has been suggested that CID can provide information on a seismic source (i.e., seismic fault region). For instance, Afraimovich et al. (2006) used an approximation of a spherical wave propagating from a point source at a constant speed and managed to show the position of a CID source in the vicinity of the epicenter of the 2003 Hokkaido
earthquake in Japan. Similar method was later successfully applied by Shults et al. (2016) to localize of the April 2015 Calbuco volcano eruptions and to estimate the onset time of the eruptions from ionospheric GNSS measurements. Liu et al. (2010) suggested a method based on the ray-tracing and the beam-forming techniques and successfully localized the epicenter of the 1999 Chi-Chi earthquake in Taiwan from ionospheric Global Positioning System (GPS) data. Lee et al. (2018) used for the first time ionosphere-based back-projection method to estimate the location of the seismic source of the 2016 Kaikoura earthquake in New Zealand.

Even closer relation between CID and a seismic source structure was shown for recent giant earthquakes with magnitudes $M_w \geq 9.0$. Heki et al. (2006) analyzed ionospheric total electron content (TEC) response to the great M9.1 2004 Sumatra earthquake and reproduced the rupture process. Astafyeva et al. (2011) used 1-Hz GPS-TEC data and, on the example of the Mw9.0 2011 Tohoku-oki earthquake, obtained for the first time the ionospheric images of seismic fault. Astafyeva, Rolland, et al. (2013) showed that ionospheric measurements can provide information on a seismic source location and even on the source dimensions within ~8 min after an earthquake in case if we detect direct acoustic waves above the epicentral area. In addition to that, Astafyeva, Rolland, et al. (2013) demonstrated that plotting standard snapshots of TEC over the epicentral area is useful to retrieve the information about the seismic source structure. Thus, for the case of the 2011 Tohoku-oki earthquake, two areas of enhanced TEC simultaneously occurred at ~150 km eastward from the epicenter ~520–530 s after the earthquake (Astafyeva, Rolland, et al., 2013). The location of these two TEC enhancements corresponded to the location of two segments of coseismic uplift as was shown by seismologists (Bletery et al., 2014; Simons et al., 2011).

It is important to emphasize that ionospheric information about seismic source can be obtained shortly after an earthquake, within ~8–9 min. In such a case, the CID information could be used for tsunami alerts in the near real time, since CID are generated by a seismic uplift that also generates tsunamis. However, while we are talking more and more often about ionosphere-based tsunami warning systems (e.g., Kamogawa et al., 2016; Savastano et al., 2017), it is now of highest importance to understand possibilities and limitations of seismo-ionospheric methods. It is especially critical knowing that our knowledge on CID generation over the epicentral area is not yet quite sufficient. Also, most of studies were devoted to giant earthquakes such as the Mw9.1 2004 Sumatra or the Mw9.0 2011 Tohoku-oki events, whereas smaller magnitude earthquakes that occur much more often but nevertheless can lead to catastrophic damages and tsunamis, received less attention from the community.

The main focus of this work is to study the possibility of ionospheric GNSS imagery for smaller earthquakes and to examine difficulties and restrictions of the suggested method. The former is done on the example of the Mw7.4 2011 Sanriku-oki earthquake by using high-rate 1-Hz ionospheric TEC data from Japanese network of ground-based GPS receivers GEONET (GNSS Earth Observation Network System).

2. The Mw7.4 Sanriku-Oki Earthquake of 9 March 2011

On 9 March 2011, at 02:45:20 UT, a large thrust earthquake of a moment magnitude 7.4 shook the middle portion of the Japan trench. With hypocenter depth of 32 km, this shallow earthquake had an epicenter at point 38.435°N, 142.842°E (https://earthquake.usgs.gov/earthquakes/eventpage/usp000hvhj#). Shao et al. (2011) calculated the hypocenter position to be at the depth of 14 km in the point with coordinates (38.34°N, 143.12°E). Seismological models estimated the seismic slip reaching up to ~2 m at ~20–40 km on the northwest from the epicenter (e.g., Shao et al., 2011; http://earthquake.usgs.gov; Figure 1a).

One of the most important seismological characteristics of an earthquake is the magnitude and the position of coseismic crustal vertical displacement that serves the source for generation of tsunamis and CID. Thomas et al. (2018) estimated the coseismic deformation pattern due to the Sanriku-oki earthquake as subsidence on the west-northwest from the epicenter and uplift on the east from the epicenter. The maximum uplift of ~0.3 m was located ~20 km from the epicenter (here shown by white cross in Figure 1a).

The Sanriku-oki earthquake caused a small tsunami runups up to ~0.6 m in Ofunato, Japan (https://www.ngdc.noaa.gov/). Note that the Sanriku-oki earthquake occurred 51 hr before the Mw9.1 Tohoku earthquake and is often referred to as the Tohoku foreshock.
3. Results and Discussions

3.1. Ionospheric Response to the Sanriku-Oki Earthquake of 9 March 2011

The dispersive property of the ionosphere makes it possible to estimate TEC from the linear combination of carrier phase and code dual-frequency GNSS measurements (e.g., Calais & Minster, 1995; Hofmann-Wellenhof et al., 2008). TEC is measured in TEC units (TECU), with 1 TECU equal to $10^{16}$ electrons/m².

In this paper, the estimated slant TEC was converted to vertical TEC (Klobuchar, 1986). The elevation cutoff was set to 15°. To extract the CID signatures, we used the running mean filtering method that works as band-pass filter in the range 0.5–6 min.

During the Sanriku-oki earthquake, several GPS satellites were visible by ground-based GPS receivers of the GEONET. However, here we focus on the near-epicentral area, and therefore, we only discuss measurements by GPS satellites G07 and G10.

Figures 2a and 2b show the geometry of GPS sounding for satellites G07 (a) and G10 (b) during the 9 March 2011 earthquake. The corresponding TEC measurements for GPS satellites G07 and G10 can be found in Figures 2c and 2d. One can see that the waveform of the observed TEC signal varies depending on the sounding position relative to the epicentral area. On the north, we mostly observe smaller amplitude signals and small TEC depletions. On the south, the TEC response shows a typical N-waveform with larger amplitude. The difference in the CID waveform with respect to the seismic source is usually explained by the impacts of the magnetic field on CID propagation and by the geometry of GPS-sounding, and has been extensively discussed in previous works (e.g., Afraimovich et al., 2001; Bagiya et al., 2017; Heki & Ping, 2005; Rolland et al., 2013).

The traveltime diagrams for observations from satellites G07 and G10 are shown in Figures 2e and 2f, respectively. We see good correlation with the earthquake’s epicenter that confirms that the observed ionospheric TEC perturbations were generated by the earthquake. From these diagrams we estimate the horizontal CID...
velocity in the near field to be ~1.1 and ~1.3 km/s for G10 and G07 observations, respectively. These values are in line with previous observations and are usually attributed to acoustic and shock-acoustic waves. However, we note that at the ionospheric latitudes the sound speed varies from ~300 m/s in the lower ionosphere to ~1000 m/s in the upper ionosphere (Figure 3c). Therefore, our observations might signify the shock origin of the observed CID.

Observations from G07 (Figure 2e) also show the occurrence of another faster perturbation starting from ~330 km from the epicenter. Its velocity is estimated as ~3.6 km/s, which is close to the speed of the Rayleigh surface wave. The Sanriku-oki earthquake generated two-mode CID as it was in the case of several other significant earthquakes (e.g., Astafyeva et al., 2009; Liu et al., 2011; Reddy & Seemala, 2015).

3.2. CID First Arrivals and the Altitude of CID Registration

To obtain the information on the seismic source from ionospheric measurements, one should first determine the first arrivals of CID over the epicentral area (Astafyeva et al., 2011; Astafyeva, Rolland, et al., 2013). The first CID arrival is defined as the moment when the TEC starts to increase (Figures 1b–1d). This can be done easily and precisely for well shaped CID, such as N-waves. Whereas, it can be difficult for more shapeless TEC variations, and it might lead to an error in the final result. Otherwise, for this method, it is also possible to use the moments of the first TEC maximums (Astafyeva et al., 2011). From the first CID arrivals or the TEC maximum points, and knowing the altitude of detection, one can obtain the ionospheric images of the seismic fault ruptured in an earthquake. Another method can be plotting TEC snapshots (Astafyeva, Rolland, et al., 2013), which is somewhat easier and faster than the first method. However, to plot the snapshots, one needs to apply a filter, and the filtering will shift the CID arrival time. Consequently, the CID arrival time will be determined with less precision.
We emphasize that both these methods will significantly rely on the altitude of CID detection (\(H_{\text{ion}}\)) in the GNSS-sounding method. \(H_{\text{ion}}\) cannot be known for certain but can be suggested from physical principles. It is known that TEC is an integral parameter equal to the total number of electrons along a line of sight between a satellite and a receiver. It is generally assumed that the TEC perturbations are concentrated around the altitude of the maximum ionosphere ionization, that is, in the ionospheric F layer. To track the TEC perturbations, the ionosphere is considered as a thin shell layer at the altitude \(H_{\text{ion}}\), so that the intersection points between a line of sight and the thin ionospheric shell that are called ionospheric piercing points (IPPs) will provide the coordinates of observed TEC disturbances. Changing the \(H_{\text{ion}}\) will change the IPP coordinates, and therefore, the choice of the \(H_{\text{ion}}\) is extremely important for the ionospheric imagery of the seismic source (Astafyeva, Rolland, et al., 2013). Some hints on the altitude of detection can be found from 3-D analysis of the GNSS-sounding geometry, including elevation angles of detection (Thomas et al., 2018). Also, comparison of the real CID arrival times with the theoretic arrival times of the acoustic waves at different altitudes may help.

For the 2011 Sanriku-oki earthquake, by using only data of satellite G07 Thomas et al. (2018) found extremely early first CID arrivals and explained them by a particular geometry of sounding at low-elevation angles. Thomas et al. (2018) found that the first ionospheric detection took place at around 130 km of altitude, which is much below the ionization maximum of 275 km as follows from the International Reference Ionosphere (IRI) model (Bilitza et al., 2017; Figure 3a). Our results here confirm that for both G07 and G10 measurements the first CID occur 470–480 s after the earthquake (Figures 1b–1d).
Considering the vertical velocity of acoustic waves, the perturbations were, most likely, indeed, detected at altitudes much lower than 275 km. Simple acoustic ray-tracing (method similar to Heki & Ping, 2005) for atmospheric conditions of 9 March 2011 (the sound speed profile presented in Figure 3c) shows that in a time period of 470–480 s, the acoustic waves above the source area will only reach the altitudes of ~140–150 km (Figure 3d). However, at these altitudes the background electron density is quite low (Figure 3a) and the background absolute TEC below this altitude reaches only 0.5–0.7 TECU (Figure 3b). Therefore, it might be doubtful that CID of any discernible amplitude can be generated at such low ionospheric background. It should be noted that the first CID arrival is the time when the CID only starts to develop, and the CID is formed at the point of the TEC maximum. By the time of the first maximums at ~510–520 s (Figures 1b–1d), the acoustic waves will reach 180–200 km (Figure 3d), with the background TEC of about 1.4–2.2 TECU (Figure 3b). With the maximum amplitude of the first detected CID of ~0.04–0.08 TECU (Figures 1b–1d), the CID then represents ~4–5% of the background, which is more credible but yet might be questionable.

In addition to the above conceptions on the theoretic arrivals of the acoustic waves and the background ionization, we can investigate how changing the altitude of CID detection will change the positions of the IPP for the Sanriku-oki case. Figures 4a–4c show the location of the first arrivals (which normally would show the location of the seismic source) at 480 s after the earthquake depending on $H_{ion}$. Here we analyze the CID position for $H_{ion}$ located at the ionization maximum of 275 km (a), at 140 km where we seem to detect the first arrivals (b) and at 190 km where we detect the first TEC maximums (c). One can see that for $H_{ion} = 275$ km the first CID is located far away from the epicentral area, while for $H_{ion} = 140$ km the first TEC perturbation is detected closer to the epicenter, but on the southwest from it. The best agreement between the source and the CID is reached for $H_{ion} = 180–190$ km (Figure 4c).

### 3.3. Acoustic and Shock-Acoustic Waves

Let us now recall that CIDs are often referred to as shock-acoustic waves rather than regular acoustic waves (e.g., Afraimovich et al., 2001, 2006; Astafyeva, Shalimov, et al., 2013; Blanc, 1985). This presumes that in the atmosphere the acoustic waves become shock-acoustic and may propagate at speeds exceeding the sound speed and, consequently, reach higher altitudes faster. The difference in the wave speed between the acoustic and shock waves will appear starting from ~100 to 120 km of altitude and will depend on the Mach number (M). Thus, for $M = 1$ at ~190 km the shock waves will be several seconds ahead of the acoustic waves (Besset & Blanc, 1994), while faster shock waves can gain several tens of seconds with respect to the acoustic waves (Daniels et al., 1960). The difference in propagation time between the two types of wave increases with altitude and at 300–400 km may reach 2–3 min. We note however that all this primarily concerns strong atmospheric sources such as explosions or underground nuclear explosions. Besides atmospheric sources, giant shallow earthquakes such as the 2011 Tohoku-oki earthquake can also produce shock waves as recently has been shown by observations and modeling (e.g., Astafyeva et al., 2011; Zettergren et al., 2011).
2017). Whereas, transformation of the acoustic waves into shock-acoustic waves for smaller amplitude earthquakes seems yet debatable.

Concerning our results on the Sanriku-oki earthquake, its moment magnitude was only 7.4, but several of our observations are difficult to explain in terms of regular acoustic waves: (1) early CID arrivals presume that the CID were detected at very low altitudes where the background TEC might be too low to produce discernible TEC perturbations; (2) from traveltime diagrams, the apparent horizontal velocities of 1.1 and 1.3 km/s exceed or largely exceed the sound speed at ionospheric altitudes, especially if the altitude of detection is low (Figure 3c); (3) the horizontal distances traveled by the CID as seen in our observations are also difficult to explain. Figures 5a–5c show TEC snapshots for $H_{ion} = 190$ km and time moments 600 s (a), 650 s (b), and 700 s (c) after the earthquakes. Comparison of the horizontal distances traveled with time by theoretic acoustic waves (Figure 3d) and those passed by real CID (Figures 5a–5c) reveals that CID generated by the Sanriku-oki earthquake traveled faster than the theoretic acoustic waves. The latter two observations can be partly explained by discrepancies in our assumptions and the real CID propagation. For instance, the fact that in reality CID propagate upward with time, whereas, for the GNSS-sounding, we use the constant altitude $H_{ion}$ for all observations, from the first CID detection to later observations.

Current results are a good demonstration that our understanding and knowledge of the CID origin and evolution are yet not quite sufficient, and they also present challenges for future works.

3.4. CID Formation Over the Epicentral Area: Ionospheric Imagery of the Seismic Source

Let us now analyze in detail the formation of CID over the epicentral area and its further evolution. Animation S1 in the supporting information shows the TEC variations around the epicentral area of the Sanriku-oki earthquake from the moment of the earthquake at 02:45:20 UT until 900 s after it. One can see that within the first ~470 s after the earthquake onset the TEC varied within ±0.05 TECU, which is in the range of the background TEC variations. Starting from ~555 s, we observe a small depletion over the area of the initial TEC increase. This TEC depletion is, most likely, the representation of the negative half-phase of the N-wave (Astafyeva, Shalimov, et al., 2013) and is often observed over the epicentral regions (e.g., Kakinami et al., 2012). From this source region both positive and negative half-phases further propagate south-westward and intensify. Starting from ~710 s after the earthquake onset, the positive phase of the CID seemed to fade, while the negative phase continued for about 200 s more.

Overall, several important findings can be retrieved from the TEC snapshots presented in Animation S1: first, and foremost, the position of the first CID arrivals corresponds to the position of the coseismic uplift on the north-northeast from the epicenter. Second, the dimensions of the ionospheric source region roughly correspond to the area of the coseismic uplift occurred due to the earthquake. Note that the Sanriku-oki
earthquake is an example of a large but not giant earthquake, and it was characterized by rather simple seismic fault zone that contained only one segment of uplift with dimensions ~45 * 40 km. For larger and much larger earthquakes, the fault is usually much more complex: it is extended and often comprises several segments (subfaults). The structure of a seismic source can be understood from seismological data, but also, as recent seismo-ionospheric results suggest, it can be done from ionospheric TEC measurements. For instance, in the case of the great M9.1 2004 Sumatra earthquake, the seismic fault was elongated for nearly ~1,300 km and consisted of six segments. Heki et al. (2006) from ionospheric GPS data managed to reconstruct the rupture process, showing contribution of each of the six segments in the observed CID. In the case of the Tohoku-oki earthquake, the source with dimensions ~350 * 150 km was located ~120–150 km eastward from the epicenter. Seismological data sets showed that the source region consisted of two main segments (Bletery et al., 2014; Simons et al., 2011), and Astafyeva, Rolland, et al. (2013) showed the same by using ionospheric 1-Hz TEC data. These examples, along with our current results, demonstrate that ionospheric TEC data can help with the reconstruction of the seismic source parameters from the ionosphere shortly after an earthquake, provided that the geometry of GNSS sounding is fortunate and the Hion is determined. Our results, therefore, could be used in the future for near–real-time ionosphere-based tsunami warning systems for smaller and giant earthquakes. It should be noted, however, that ionospheric imagery of seismic source is only possible while using high-rate ionospheric data. Standard data sampling for GNSS of 30 s or 10–15 s might not provide the desired results because of low resolution. For instance, we attempted to obtain images for the M7.8 2015 Nepal earthquake by using standard 30-s GPS data but we failed.

4. Conclusions
In this work, by using 1-Hz data from ground-based GPS receivers of the GEONET, we analyzed the ionospheric response to the Mw7.4 Sanriku-oki earthquake of 9 March 2011. Two GPS satellites, G07 and G10, sounded the epicentral area and showed the occurrence of TEC enhancement on the east-northeast from the epicenter starting from 470 – 480 s (~7.8–8 min) after the earthquake. The location of this initial TEC increase corresponds to the location of the coseismic crustal uplift that occurred due to the earthquake.

The main difficulty of the method of the GNSS-based ionospheric imagery lies in an unknown altitude of ionospheric detection Hion. Here we showed that knowing the real time of the first CID arrivals together with the theoretical arrival time of the acoustic waves helps to overcome this difficulty. Overall, our results confirm that despite several difficulties, high-rate ionospheric GPS data can be used for determining the seismic source parameters from the ionosphere. This method should work for both giant and smaller/moderate earthquakes.

Finally, our observations raise several fundamental questions, merely, on the acoustic or shock-acoustic nature of CID generated by smaller earthquakes. Can moderate earthquake generate shock waves?—this question is yet to answer.

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