Magneto-Optics of Excitons Interacting with Magnetic Ions in CdSe/CdMnS Colloidal Nanoplatelets

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ABSTRACT: Excitons in diluted magnetic semiconductors represent excellent probes for studying the magnetic properties of these materials. Various magneto-optical effects, which depend sensitively on the exchange interaction of the excitons with the localized spins of the magnetic ions can be used for probing. Here, we study core/shell CdSe/(Cd,Mn)S colloidal nanoplatelets hosting diluted magnetic semiconductor layers. The inclusion of the magnetic Mn2+ ions is evidenced by three magneto-optical techniques using high magnetic fields up to 15 T: polarized photoluminescence, optically detected magnetic resonance, and spin-flip Raman scattering. We show that the holes in the excitons play the dominant role in exchange interaction with magnetic ions. We suggest and test an approach for evaluation of the Mn2+ concentration based on the spin−lattice relaxation dynamics of the Mn2+ spin system.

KEYWORDS: diluted magnetic semiconductors, CdSe nanoplatelet, colloidal nanocrystals, magneto-optics, spin-flip Raman scattering, optically detected magnetic resonance

Incorporation of magnetic ions in colloidal nanocrystals (NCs) opens exciting opportunities for the engineering of spintronics devices.1−4 The underlying idea to exploit the strong sp−d exchange interactions of electrons and holes with the localized spins of magnetic ions originates from the physics of diluted magnetic semiconductors (DMSs).5 This research direction was established first for bulk DMS materials and later was successfully extended for epitaxially grown DMS heterostructures, including quantum wells and quantum dots.6,7 In colloidal nanostructures, it is still at an early stage, while several important results have been already achieved. The giant Zeeman splitting was demonstrated by measuring the magnetic circular dichroism,8−11 including the photoinduced magnetism in Ag-doped CdSe NCs,12 and evidenced by polarized photoluminescence (PL) in external magnetic fields.13−15 The exchange interaction of excitons with Mn2+ ions was proven by optically detected magnetic resonance (ODMR).16 Magnetic polaron formation was reported,3,20−22 and the influence of Mn2+ spin fluctuations was considered.23

Magneto-optical studies of the exciton emission, its giant Zeeman splitting and polarization, are a valuable tool for investigation of DMS nanostructures. There is, however, a limitation for the parameters of DMS NCs to provide efficient exciton PL. The Mn2+ ions have an absorption band at the energy of about 2.1 eV associated with the internal transition 6A1 → 4T1; the corresponding 4T1 → 6A1 emission is located at about 2.0 eV. This means that in (Cd,Mn)Se NCs, the exciton resonance should be considerably detuned from this energy, because the efficient energy transfer to the Mn2+ ions would otherwise provide a nonradiative recombination channel for the excitons, quenching their emission. For this reason, (Cd,Mn)Se spherical NCs with large diameters were synthesized in order to keep the exciton emission energy below 2.1 eV.11,13,21 Nanoplatelets (NPLs) are an emerging class of colloidal nanocrystals, which are atomically flat with several monolayer thickness, resembling free-standing quantum wells.24 NPLs with magnetic Mn2+ ions were synthesized in 2015,16 providing...
remarkable opportunities for wave function engineering. The Mn2+ ions were incorporated in the NPL cores or shells.

In this paper, we study the magneto-optical properties of core/shell CdSe/Cd1−xMnx S NPLs, which arise from excitons interacting with the magnetic ions. Three experimental approaches are used: (i) polarized PL in external magnetic fields, (ii) optically detected magnetic resonance of the Mn2+ ions, and (iii) spin-flip Raman scattering. We measure the spin–lattice relaxation dynamics of the Mn2+ spin system and suggest an approach for evaluation of the Mn2+ concentration.

Four NPL samples were grown for this study, see refs 16, 29, and 30 and Supporting Information S1 for details. All of them have a 2-monolayer thick CdSe core and 4-monolayer thick shells cladding the core. The reference sample #0 has nonmagnetic CdS shells, and the other three DMS NPLs have Cd1−xMnx S shells with Mn2+ concentrations ranging from 0.009 to 0.029. The sample parameters are given in Table 1.

Table 1. Parameters of the Studied CdSe/CdS and CdSe/Cd1−xMnx S NPLs

| sample # | Mn2+ content from ICP-MS (ppm) | rSLR (μs) | Mn2+ content from ODMR (ppm) | ΔEg (meV) |
|----------|--------------------------------|-----------|------------------------------|-----------|
| 0        | 0                              | -         | 0.009                        | 1.7       |
| 1        | 0.012                          | 405       | 0.009                        | 1.6       |
| 2        | 0.019                          | 350       | 0.010                        | 1.8       |
| 3        | 0.050                          | 20        | 0.029                        | 1.9       |

Note that the Mn2+ concentrations obtained by inductively coupled plasma mass spectrometry (ICP-MS) measurements differ from the values that we evaluate from the spin–lattice relaxation dynamics. We are convinced that the latter values are more reliable and we use them in the paper.

RESULTS AND DISCUSSION

Specifics of DMS Heterostructures. The band structure of the CdSe/Cd1−xMnx S NPLs is shown schematically in Figure 2a. The CdSe core with zincblende lattice (Figure S1) has the bandgap energy Eg, CdSe = 2.50 eV and is sandwiched between shells with Eg, CdS = 2.50 eV. Note that the Eg, CdSe = 1.84 eV used in refs 19 and 26 corresponds to the wurtzite lattice. The conduction and valence band offsets between CdSe and CdS are not precisely known. However, the valence band offsets reported in literature are large, so that the hole is believed to be confined in the CdSe core. The reported conduction band offsets range from 300 to 0 meV, and this value depends on the crystal structure, NC size, lattice strain, and temperature. Due to the quite weak confinement, the electron wave function leaks into the CdS shell (for references, see ref 32). The electron and hole wave functions are centered in the nonmagnetic CdSe core and only partially penetrate into the DMS shell. For this reason, all exchange effects in the studied DMS NPLs are expected to be reduced compared to bulk DMSs with the same Mn2+ concentration. Quantum mechanical calculations give an estimate of the electron wave function fraction in the shell about 60% and the hole fraction about 30%, see Supporting Information S5.

There are several factors that need to be taken into account for evaluation of the strength of the exciton and carrier exchange interactions with the Mn2+ spins in CdSe/Cd1−xMnx S NPLs:

(i) Penetration of the electron and hole wave functions into the DMS shells. Note that in bulk II–VI DMSs, the exchange interaction of holes is 4–8 times stronger than that of the electrons. Correspondingly, the holes provide the dominating contributions to the magneto-optical effects, like the giant Zeeman splitting of exciton states, Faraday rotation, formation of exciton magnetic polarons, etc.

(ii) Modification of the electron exchange constant α by strong quantization. α is reduced with increasing confinement and can even change its sign.

(iii) Variations of the magnetic properties of the Mn2+ spin system, which are controlled by the Mn2+–Mn2+ interactions and are different in bulk DMSs and in thin DMS layers or at the interfaces between DMS and nonmagnetic layers, because of different statistics of neighboring Mn2+ spins.

Therefore, it is a challenging task to account properly for the contributions of these factors to the magneto-optical properties of the studied NPLs. As a result, one can not use most of the established approaches in DMS physics for evaluation of the Mn2+ content by means of magneto-optical techniques.

Time-Integrated and Time-Resolved Photoluminescence. Figure 1a shows PL spectra of CdSe/CdS (sample #0) and CdSe/Cd0.991Mn0.009S (sample #1) NPLs. Both spectra are very similar to each other, so that implementation of a small Mn2+ concentration does not change the PL. The emission lines of both samples are centered at 2.127 eV (red arrow) and have

![Figure 1](https://example.com/figure1.png)

Figure 1. (a) PL spectra of CdSe/CdS (sample #0, pink) and CdSe/Cd0.991Mn0.009S (sample #1, green) NPLs in B = 0 T. (b) PL decay traces of sample #0 (pink) and sample #1 (green) NPLs, measured at their PL maxima of 2.127 eV. (c) PL decay curves of CdSe/Cd0.991Mn0.009S NPLs (sample #1) at various detection energies shown by the arrows in panel (a) with the same color code. Inset: Spectral dependence of the average decay time (τ) in sample #1. (d,e) PL decay at 2.127 eV measured in magnetic fields B = 0 T (green) and 15 T (red) in samples #1 and #0. All measurements performed at T = 4.2 K.
Figure 2. (a) Schematic diagram of the electron and hole wave functions (blue and red contours) in CdSe/Cd_{0.991}Mn_{0.009}S NPLs for the conduction valence band offset 0.15 eV. (b) PL spectra of the σ’ (red) and σ’’ (blue) polarized components in CdSe/CdS NPLs (sample #0, bottom) and CdSe/Cd_{0.991}Mn_{0.009}S NPLs (sample #1, top) at T = 4.2 K, B = 3 T (left), and 15 T (right). (c) Magnetic field dependence of the DCP in sample #0 (pink) and sample #1 (green).

Full widths at half-maximum of about 100 meV, which is typical for core/shell NPLs.37 As the PL is close to the 4^6T_1 → 6^4A_1 transition of the Mn^{2+} ions at 2.1 eV from our first task is to identify the origin of the emission from CdSe/Cd_{0.991}Mn_{0.009}S NPLs and to prove that it is dominated by exciton recombination. The similarity of the PL spectra of nonmagnetic and DMS NPLs gives a first hint for that.

The recombination dynamics can also be used for the identification of the origin of the emission. It is known that at liquid helium temperatures, the decay of the Mn^{2+} emission via the 4^6T_1 → 6^4A_1 transition is very slow, occurring on time scales in the 10–500 μs range in bulk DMSs38,39 like (Cd,Mn)Te, (Zn,Mn)Te, and (Zn,Mn)S, and is 270 μs in (Cd,Mn)Se colloidal quantum dots.40 The exciton recombination dynamics is by a few orders of magnitude faster, happening for neutral excitons in the range of 1 ns to 1 μs, depending on the relative involvement of bright and dark exciton states or of a few nanoseconds for charged excitons (trions).37,41,42

The time-resolved recombination dynamics measured at the PL maxima in samples #0 and #1 are shown in Figure 1b. In both cases, the decay of the PL intensity takes place within 300 ns being 3 orders of magnitude faster than the recombination dynamics of Mn^{2+} ions. This allows us to conclude that the dominant part of the emission in CdSe/Cd_{0.991}Mn_{0.009}S NPLs is provided by exciton recombination and the Mn^{2+} emission is very weak, if present at all. The two other DMS samples have similar properties.

As it is common for the colloidal nanocrystals, the recombination dynamics in the studied NPLs do not show a monoexponential decay. For example, the decays at the PL maxima, shown in Figure 1b, require a fit with a three-term exponential function for a good description: \( I(t) = A_1 \exp(-t/\tau_1) + A_2 \exp(-t/\tau_2) + A_3 \exp(-t/\tau_3) \). The three decay times are \( \tau_1 = 3 \) ns, \( \tau_2 = 11 \) ns, and \( \tau_3 = 56 \) ns for sample #0 and \( \tau_1 = 3 \) ns, \( \tau_2 = 12 \) ns and \( \tau_3 = 45 \) ns for sample #1. Note that they are close to each other in these nonmagnetic and DMS NPLs.

The spectral dependence of the PL dynamics in CdSe/Cd_{0.991}Mn_{0.009}S NPLs is given in Figure 1c. The general trend is that the decay times increase with decreasing emission energy. This is clearly seen in the inset of Figure 1c, where the spectral dependence of the average decay time (\( \tau \)) is given. \( \tau \) is calculated as \( \tau = \tau_1 \nu_1 + \tau_2 \nu_2 + \tau_3 \nu_3 \), where \( \nu_i = A_i/\nu(A_i \tau_1 + A_2 \tau_2 + A_3 \tau_3) \). The average decay time increases from 2 up to 70 ns from the high- to the low-energy tail. The nonmagnetic sample demonstrates the similar spectral dependence (Figure S2), which proves that it is not due to the Mn^{2+} emission. Such behavior is typical for ensembles of colloidal nanocrystals with an efficient Förster energy transfer.43,44

Further more, the recombination dynamics are weakly affected by external magnetic fields. This is shown in Figure 1d,e, where the PL decays at the emission maximum are compared for \( B = 0 \) and 15 T.

Note that the character of the recombination dynamics at low temperatures in colloidal NPLs and its dependence on magnetic field allows one to identify whether the emission is contributed by neutral or by charged excitons.37,41,42 For example, at \( T = 4.2 \) K, the trion emission in CdSe/CdS NPLs with thick shells is monoexponential with a decay time of 3 ns and is independent of magnetic field. Contrary to that, the decay of neutral excitons in CdSe NPLs has a biexponential decay with a very fast initial component of 20 ps and a long component of 80 ns, which shortens with increasing magnetic field.

The recombination dynamics in the NPLs studied in this paper do not clearly correspond to either neutral or charged exciton behavior, but are rather superpositions of both. Additionally, for resonant excitation, we clearly observe emission from dark excitons (Figure 4a). The bright-dark exciton energy splitting, \( \Delta E_{AD} \), ranges between 1.6 and 1.9 meV (see below). Therefore, at \( T = 4.2 \) K, the bright state has about 1% population in thermal equilibrium and should contribute to the emission. We also detect electron spin flips, which means that some of the NPLs are negatively charged, that is, they may contain negatively charged excitons (Figure 4a). From all these findings, we conclude that the PL is contributed by a recombination of neutral (bright and dark) and charged excitons. More details are given in the Supporting Information S4.

**Polarized Photoluminescence in the Magnetic Field.** This technique, which exploits the exciton (trion) spin polarization on their Zeeman split sublevels, is a sensitive tool to measure small spin splittings comparable with the thermal energy \( k_B T \), where \( k_B \) is the Boltzmann constant.37,45,46 The experiment is relatively easy in realization, but requires liquid helium temperatures and strong magnetic fields of 10–15 T or even up to 30–65 T to gather sufficient information on the linear dependence of the circular polarization degree of PL, \( P_e(B) \), on...
magnetic fields in weak fields, until it reaches saturation in high magnetic fields, $P_{\sigma^+}$. The degree of circular polarization (DCP) is defined as $P_{i} = (I_i - I')/(I_i + I')$, where $I_i$ and $I'$ are the PL intensities of the $\sigma^+$ and $\sigma^-$ circularly polarized components, respectively. The magnetic field is applied in the Faraday geometry, that is, parallel to the emission wave vector direction.

Figure 2b shows polarized PL spectra of the nonmagnetic sample #0 (bottom) and Mn-doped sample #1 (top), measured in magnetic fields $B = 3$ and 15 T. One can clearly see the difference between DCP in nonmagnetic and DMS NPLs. First, they have opposite signs. In CdSe/CdS NPLs $P_{\sigma^-} < 0$, the absolute value increases with growing magnetic field about monotonically and saturates above 12 T (Figure 2c). At $B = 15$ T, it reaches $P_{\sigma^-} = -0.47$. This behavior is similar to what was reported for thick-shell CdSe/CdS NPLs (see Figure 3c in ref 37), where the emission was provided by negatively charged excitons.

In the DMS sample $P_{\sigma^+} > 0$, it increases fast, reaching a plateau value of +0.22 at $B = 4$ T, and then slowly decreases in higher magnetic fields. The $P_{\sigma^+}$ sign reversal in II–VI DMS materials, compared to the nonmagnetic reference, is clear evidence of the exchange interaction of charge carriers with the Mn$^{2+}$ ions. It is provided by the signs of the exchange constants in the conduction ($\alpha > 0$) and valence bands ($\beta < 0$). More details are given in the Supporting Information S6.

**Analysis of Polarized Photoluminescence.** The exciton and trion DCP can be written as

$$P_{\sigma^+}(B) = -P_{\sigma^+}^{sat}\frac{\tau}{\tau + \tau_s}\frac{\Delta E_Z(B)}{2k_B T}$$

where $\Delta E_Z(B)$ is the Zeeman splitting, $\tau$ is the lifetime, $\tau_s$ is the spin relaxation time, and $P_{\sigma^+}^{sat}$ is the saturation degree of the $\sigma^+$ circularly polarized components.

In nonmagnetic samples, the intrinsic exciton Zeeman splitting is

$$\Delta E_{ZX}(B) = g_x\mu_B B$$

where $g_x$ is the exciton $g$-factor, and $\mu_B$ is the Bohr magneton. Accounting for the specifics of the bright and dark excitons is considered in Supporting Information S6.

In DMS samples, an additional term, $E_{exch,X}(B)$, describing the exciton exchange interaction with the Mn$^{2+}$ spins has to be added

$$\Delta E_{ZX}(B) = g_x\mu_B B + E_{exch,X}(B)$$

Note that $E_{exch,X}(B)$ is controlled by the exchange interaction of both electron and hole composing the exciton with the Mn$^{2+}$ ions and therefore depends on the overlap of the electron and hole wave functions with the (Cd,Mn)S shells.

For the negative trion, being composed of two electrons and one hole, the Zeeman splitting is determined by the hole wave functions with the (Cd,Mn)S shells.
\[ \Delta E_{Z,h}(B) = -3g_e \mu_B B \]

where \( g_e \) is the hole g-factor. In DMS samples
\[ \Delta E_{Z,h}(B) = -3g_e \mu_B B + E_{\text{exch},h}(B) \]

\( E_{\text{exch},h}(B) \) is determined by the exchange interaction of the hole with the Mn\(^{2+} \) ions. Here we use the definition of the hole g-factor sign that is commonly used for colloidal nanocrystals.\(^{37,38}\)

In the frame of this convention, the intrinsic hole Zeeman splitting provided by the negative hole g-factor (\( g_e < 0 \)) is in competition with the hole exchange splitting determined by \( B < 0 \). On the other hand, for the conduction band electron, both the intrinsic Zeeman splitting and the hole exchange interaction contribute to the total Zeeman splitting provided by the negative hole g-factor. Here we use the definition of the hole g-factor sign that is commonly used for colloidal nanocrystals.\(^{37,47}\)

As one can see from Table 1, the Mn\(^{2+} \) concentration measured by the ICP-MS method is in good agreement with our data for CdSe/Cd\(_{1-x}\)Mn\(_x\)S NPLs. Table 1 shows that the resonant heating of the Mn\(^{2+} \) spin system can be detected by several effects: (i) the decrease of the exciton giant Zeeman splitting, resulting in a spectral shift of the exciton emission line, (ii) the decrease of the circular polarization degree induced by the magnetic field, and (iii) the redistribution of the emission intensity between the exciton line and the Mn\(^{2+} \) emission band. Recently, ODMR measurements were performed for CdSe/Cd\(_{1-x}\)Mn\(_x\)S NPLs.\(^{19}\)

Figure 3a shows the intensities of the \( \sigma^+ \) and \( \sigma^- \) PL components of the CdSe/Cd\(_{0.996}\)Mn\(_{0.004}\)S NPLs (sample #1), measured versus magnetic field without and with microwaves. As discussed above, the \( \sigma^+ \) component has a higher intensity due to the stronger thermal population of the excitons (trions) on the associated Zeeman sublevels split in magnetic field. Without microwaves, the intensities of these components change smoothly with magnetic field, following the DCP trend shown in Figure 2c. In the presence of 59.6 GHz microwave radiation, two sharp resonances are observed at \( B = 2.130 \) T. The resonant decrease of the \( \sigma^+ \) intensity and the correlated increase of the \( \sigma^- \) intensity evidence heating of the Mn\(^{2+} \) spin system, which accordingly decreases the exciton (trion) giant Zeeman splitting and the exciton (trion) DCP.\(^{35,50}\) The PL intensity variations normalized to the relative PL intensities without microwaves (\( I \)) are shown in more detail in Figure 3b. They represent broad peaks with a width of \( \Delta B = 40 \) mT and are centered at \( B = 2.130 \) T corresponding to a g-factor of 1.999 \( \pm 0.005 \). This g-factor matches with the Mn\(^{2+} \) value of \( g_{\text{Mn}} = 2.01 \), reported for ZnS:Mn\(^{2+} \) and CdTe:Mn\(^{2+} \) in electron spin resonance measurements.\(^{51,52}\)

The spin–lattice relaxation (SLR) dynamics of the Mn\(^{2+} \) spin system can be measured by modulating the microwave radiation between on and off and time-resolved detection of the changes induced thereby, reflecting cooling or heating of the Mn\(^{2+} \) spins. An example of such a measurement for CdSe/Cd\(_{0.996}\)Mn\(_{0.004}\)S NPLs is shown in Figure 3c. Here, the red line is an exponential fit with the characteristic spin–lattice relaxation time \( \tau_{\text{SLR}} = 405 \) \( \mu \)s. Similar measurements performed for samples #2 and #3 give 350 and 20 \( \mu \)s, respectively (Table 1).

As we discussed above, most of the magneto-optical approaches that are commonly used for evaluation of the Mn\(^{2+} \) concentration in bulk DMSs cannot be directly applied to CdSe/Cd\(_{1-x}\)Mn\(_x\)S NPLs. We suggest that a quite accurate evaluation can be achieved from the spin–lattice relaxation time \( \tau_{\text{SLR}} \). It is known that the \( \tau_{\text{SLR}} \) of the Mn\(^{2+} \) ions in II–VI semiconductors has a very strong dependence on the Mn\(^{2+} \) concentration, which covers about 5 orders of magnitude from 1 ms down to 10 ns with increasing \( x \) from 0.004 up to 0.11, see Figure 3e, where the data from Figure 8.10 in ref 35 are reproduced. This strong dependence arises from the quenching of the orbital momentum of the d-electrons in the Mn\(^{2+} \) ion, that is, it has zero orbital momentum (\( L = 0 \)) and does not interact with the phonon system. The only mechanisms that provide spin–lattice relaxation for the Mn\(^{2+} \) ions are given by the Mn\(^{2+} \)–Mn\(^{2+} \) interactions, which obviously are strongly dependent on the number of neighboring Mn\(^{2+} \) ions and the distances between them, which in turn strongly change with increasing Mn\(^{2+} \) concentration.

In the case of diluted magnetic semiconductors, the resonant microwave heating of the Mn\(^{2+} \) ions increases the Mn\(^{2+} \) spin temperature \( T_{\text{spin}} \), and, consequently, reduces the Mn\(^{2+} \) spin polarization \( (S_{\text{Mn}}) \). These changes can be detected optically via the excitons or trions interacting with the Mn\(^{2+} \) spins, see Figure 3d. The application of the ODMR technique to quantum well structures based on (Zn,Mn)Se DMSs is discussed in refs 35, 49, and 50. There it was shown that the resonant heating of the Mn\(^{2+} \) spin system can be detected by several effects: (i) the decrease of the exciton giant Zeeman splitting, resulting in a spectral shift of the exciton emission line, (ii) the decrease of the circular polarization degree induced by the magnetic field, and (iii) the redistribution of the emission intensity between the exciton line and the Mn\(^{2+} \) emission band. Recently, ODMR measurements were performed for CdSe/Cd\(_{1-x}\)Mn\(_x\)S NPLs.\(^{19}\)
Figure 4. (a) Raman spectrum for the circularly copolarized configuration in Faraday geometry for the nonmagnetic CdSe/CdS NPLs (sample #0). $E_{\text{exc}} = 2.165$ eV, $P_{\text{exc}} = 0.2$ W/cm$^2$, $T = 1.6$ K, $B = 0$ and 8 T. (b) Magnetic field dependence of the absolute Stokes energy shifts of the $n = 1$ Mn$^{2+}$ resonance in CdSe/Cd$_{0.991}$Mn$_{0.009}$S (sample #1, orange squares) and of the electron spin flip in CdSe/CdS NPLs (sample #0, green circles) in Faraday geometry. Lines are linear fits to the data. (c) Magnetic field dependence of the relative Raman shifts of all detectable Mn$^{2+}$ resonances in CdSe/Cd$_{0.99}$Mn$_{0.01}$S NPLs in Voigt geometry. (d) Mn$^{2+}$ spin scattering spectra for the copolarized configuration in Faraday geometry for the CdSe/Cd$_{0.991}$Mn$_{0.009}$S (sample #1, pink) and CdSe/Cd$_{0.99}$Mn$_{0.01}$S (sample #2, blue) NPLs. $E_{\text{exc}} = 2.151$ eV, $P_{\text{exc}} = 1.6$ W/cm$^2$, $B = 4$ T, $T = 1.6$ K. In Faraday geometry up to 7 (3) Mn$^{2+}$ resonances are observed in the Stokes (anti-Stokes) spectral ranges.

Spin-Flip Raman Scattering. The SFRS spectroscopy is a sophisticated tool to investigate the Zeeman splittings of carriers (electrons or holes), excitons, or magnetic ions. It provides detailed information about their spin structure and spin interactions. The polarization properties of the SFRS lines deliver information on the symmetries of the involved states and allow one to identify the responsible flip mechanisms. In SFRS, the Zeeman splitting is obtained from the Raman shift, which is equal to the energy shift between the laser photon energy and the energy of the scattered light. The technique was successfully used for investigation of the exchange interactions of carriers and excitons with the magnetic ions in DMS bulk samples\textsuperscript{37,57} and quantum well structures.\textsuperscript{54} We found that in layers with a thickness of 3 monolayers and larger, the SLR times can be longer by a factor of 5, which corresponds to a factor 2 underestimation of the Mn$^{2+}$ concentration.

No electron spin-flip is detected; instead, a set of equidistant lines is observed. Up to seven lines in the Stokes and up to three lines in the anti-Stokes energy range can be resolved. All these lines shift linearly with magnetic field (see Figure 4c), following the equation $\Delta E = n g_{\text{eff}} \mu_B B$, where $n$ is an integer number. An accurate evaluation of $g_{\text{Mn}} = 2.01 \pm 0.03$ is obtained from the fit of the line with $n = 1$, shown in Figure 4b by orange squares. This $g$-factor matches well with the Mn$^{2+}$ $g$-factor of 2.01.\textsuperscript{45,52} Hence, we conclude that the measured Raman signals have to be attributed to spin flips of the Mn$^{2+}$ ions interacting with the photogenerated exciton. We measured the spectral dependence of the Raman signal intensities. The maximal signal is reached when the laser is in resonance with the exciton. This shows that the exciton serves as an intermediate scattering state, which resonantly enhances the Raman cross-section.

The Raman signal is detected in all four combinations of circular polarizations of excitation and detection. The relative intensities ($I^+/I^- = |I^+/I^-|$) of the Mn$^{2+}$ SFRS lines depend strongly on the Mn$^{2+}$ concentration. Here $I^\pm$ means $\sigma^+$-polarized excitation and $\sigma^-$-polarized detection. These intensities on the Stokes side for $n = 1$ at $B = 4$ T are given by (1/0.95/0.99/0.95) for CdSe/Cd$_{0.991}$Mn$_{0.009}$S (sample #1), (1/0.75/0.84/0.62) for CdSe/Cd$_{0.99}$Mn$_{0.01}$S (sample #2), and (1/0.33/0.42/0.18) for CdSe/Cd$_{0.971}$Mn$_{0.028}$S (sample #3). One can conclude that the optical selection rules become more distinct with increasing Mn$^{2+}$ concentration and the Mn$^{2+}$ lines become more dominant for $\sigma^+$-polarized excitation and detection.

The observation of multiple spin flip Mn$^{2+}$ lines was reported also for (Cd,Mn)Te-based quantum wells, where up to 15 spin-flip lines were observed.\textsuperscript{44} A mechanism for these flips was suggested in ref \textsuperscript{54} and a corresponding model description was developed in refs 34, 59. The key point of this model is the anisotropic spin of the heavy-hole in a two-dimensional
nanostructure. In an external magnetic field, the Mn$^{2+}$ spins are polarized along the field direction. When the spin of the photogenerated hole is not parallel to the magnetic field (for simplicity the case when it is perpendicular to the field can be considered), the Mn$^{2+}$ spins are influenced by the external field $\mathbf{B}$ and by the hole exchange field $\mathbf{B}_{\text{exc}}$. The total magnetic moment of all Mn$^{2+}$ spins within the hole localization volume, $I_{\text{tot}}$, precesses about the total field $\mathbf{B} + \mathbf{B}_{\text{exc}}$. When the exciton recombines, i.e., scatters, the projection of $I_{\text{tot}}$ on $\mathbf{B}$ differs from the initial value by a multiple of the energy of the $n=1$ Mn$^{2+}$ spin-flip. Note that the electron with an isotropic spin does not support this mechanism. Therefore, we can conclude that in the studied DMS NPLs the holes have sufficient wave function overlap with the shell Mn$^{2+}$ spins for providing multiple SFRS. This is in line with our conclusions from the DCP data analysis.

NPLs have a close analogy to quantum wells and the model approach suggested for quantum wells can be directly applied also here. The only specifics, which need to be accounted for, are the varying orientations of the NPLs in an ensemble measurement. As we have noticed above, the condition for observation of multiple Mn$^{2+}$-flips is the noncollinearity of $\mathbf{B}$ and $\mathbf{B}_{\text{exc}}$. This means that in quantum wells the effect should be absent in the Faraday geometry, where the magnetic field is parallel to the structure growth axis. In DMS NPLs we observe the same amount of higher order spin scattering resonances in Faraday and Voigt geometry. We explain this result by the random orientation of the NPLs in the studied ensembles, leading to the situation that in any configuration a fraction of NPLs fulfills the condition for multiple Mn$^{2+}$-flips. It is worthwhile to note that the model developed for the exciton, namely for the hole in the exciton, can be readily applied for the negatively charged exciton, as the hole spin acts similar on Mn$^{2+}$ ions in both cases.

**CONCLUSIONS**

In conclusion, we have demonstrated the exchange interaction of excitons (trions) with the Mn$^{2+}$ ions in CdSe/Cd$_{1−x}$Mn$_x$S core/shell nanoplatelets by means of polarized PL, optically detected magnetic resonance and spin-flip Raman scattering. One can conclude that these structures can be studied in detail by these experimental approaches that were established for diluted magnetic semiconductors. In particular, assessment of the dynamics for spin–lattice relaxation gives accurate estimates for the Mn$^{2+}$ ion concentration. Our studies may help to functionalize colloidal DMS nanocrystals as magnetic or magneto-optical markers.

**METHODS**

**Magneto-optical measurements.** The NPLs were dropcasted on a substrate and mounted in a titanium sample holder on top of a three-axis piezo-positioner and placed in the variable temperature insert (4.2−70 K) of a liquid helium bath cryostat equipped with a superconducting solenoid (magnetic fields up to 15 T). The measurements were performed in the Faraday geometry (light excitation and detection parallel to the magnetic field direction). The PL was excited with a diode laser (photon energy 3.06 eV, wavelength 405 nm) in continuous-wave or pulsed mode (pulse duration 50 ps, pulse repetition rate 500 kHz) with a weak average excitation density of 0.5 mW/cm$^2$. The PL was dispersed with a 0.5-m spectrometer and detected either by a liquid-nitrogen-cooled charge-coupled-device (CCD) camera or a Si avalanche photodiode connected to a conventional time-correlated single-photon counting system. The instrumental response time was about 200 ps. The PL circular polarization degree was analyzed by a combination of a quarter-wave plate and a linear polarizer.

**Spin-flip Raman scattering.** The samples were mounted strain free inside the variable temperature insert of a magnet cryostat, which provided magnetic fields up to 10 T. The temperature was set to 1.8 K. The backscattering experiments were performed in Faraday geometry ($θ=0°$) or in tilted geometries up to $θ=90°$, corresponding to the Voigt geometry, where the magnetic field and the normal to the sample substrate enclose the angle $θ$. The NPLs were excited by a single frequency dye laser (Matisse DS), whose actual wavelength was measured and monitored by a fiber-coupled wavelength-meter device. The laser power was stabilized by a liquid-crystal variable attenuator. Unless specified otherwise, the power was set to about 0.2 W/cm$^2$ at the sample surface. In order to ensure a stable detection position on the sample surface, each sample was covered by a mask having a hole of 1 mm diameter and the central part with $100 × 100 \mu$m$^2$ size of the illuminated sample area was selected by a cross slit. The NPL emission was spectrally dispersed by a double monochromator (U1000) equipped with a Peltier-cooled GaAs photomultiplier. The SFRS spectra were measured in close vicinity of the laser line with photon energy $E_{\text{exc}}$. The spin-flip signals were shifted from the laser energy by the Zeeman splitting of the involved spin state, either to lower (Stokes shift, $E_{\text{exc}}−|g|μ_B B$) or higher energies (anti-Stokes shift, $E_{\text{exc}}+|g|μ_B B$).

**Optically detected magnetic resonance.** The ODMR technique used in this study was described in detail in ref 49. The ODMR spectrometer consisted of a 60 GHz all-solid-state microwave oscillator (photon energy of 0.249 meV) with a tuning range from 59.05 to 60.55 GHz and an output power of up to 100 mW. The output power of the oscillator could be varied by up to 40 dB attenuation level. The oscillator could operate either in continuous-wave mode or in a periodically pulsed mode with an on−off transition time of about 3 ns at more than 60 dB dumping level. The sample was mounted in a cylindrical H$_{011}$ microwave cavity with a low Q-factor of about 600. The cavity had two orthogonal pairs of apertures with a conic cross-section for sample illumination and collecting the sample emission. The cavity was placed in the variable temperature insert of a magnet cryostat, the measurements were performed at $T=1.8$ K. The sample in the cavity was excited by a 405 nm ($E_{\text{exc}}=3.06$ eV) semiconductor laser in cw mode with 0.5 mW power, focused into a spot with a diameter of 400 μm. The PL was collected in backscattering geometry and detected with a 0.5-m grating monochromator and a CCD camera. Magnetic fields up to 7 T were applied in the Faraday geometry. For time-resolved ODMR measurements a photon counter based on an avalanche photodiode was used, the temporal resolution was 30 ns.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsnano.0c04048.

Additional information on synthesis details, XRD data, spectrally resolved PL decays, exciton bright-dark splitting, calculation of the band structure in core/shell NPLs, modeling of the exciton exchange interaction with Mn$^{2+}$ ions, Zeeman splitting and polarization degree for the bright and dark excitons and negative trions (PDF)

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REFERENCES

(1) Efros, Al. L.; Rashba, E. I.; Rosen, M. Paramagnetic Ion-Doped Nanocrystal as a Voltage-Controlled Spin Filter. Phys. Rev. Lett. 2001, 87, 206601.
(2) Beaulac, R.; Archer, P. I.; Ochsenbein, S. T.; Gamelin, D. R. Mn2+-Doped CdSe Quantum Dots: New Inorganic Materials for Spin-Electronics and Spin-Photonics. Adv. Funct. Mater. 2008, 18, 3873–3891.
(3) Muckel, F.; Barrows, C. J.; Graf, A.; Schmitz, A.; Erickson, C. S.; Gamelin, D. R.; Bacher, G. Current-Induced Magnetic Polars in a Colloidal Quantum-Dot Device. Nano Lett. 2017, 17, 4768–4773.
(4) Moro, F.; Fielding, A. J.; Turyanska, L.; Panaté, A. Realization of Universal Quantum Gates with Spin-Qudits in Colloidal Quantum Dots. Adv. Quantum Technol. 2019, 2, 1900017.
(5) Furdyna, J. K. Diluted Magnetic Semiconductors. J. Appl. Phys. 1988, 64, R29–R64.
(6) Furdyna, J. K.; Kossut, J. In Diluted Magnetic Semiconductors; Furdyna, J. K., Kossut, J., Eds.; Semiconductors and Semimetals; Academic Press: London, 1988; Vol. 25.
(7) Gaj, J. A.; Kossut, J. In Introduction to the Physics of Diluted Magnetic Semiconductors; Kossut, J., Gaj, J. A., Eds.; Springer Series in Materials Science; Springer Verlag: Berlin, Heidelberg, 2010.
(8) Hoffmann, D. M.; Meyer, B. K.; Ekimov, A. I.; Merkulov, I. A.; Efros, Al. L.; Rosen, M.; Couino, G.; Gacoin, T.; Boilot, J. P. Giant Internal Magnetic Fields in Mn Doped Nanocrystal Quantum Dots. Solid State Commun. 2000, 114, 547–550.
(9) Norris, D. J.; Yao, N.; Charnock, F. T.; Kennedy, T. A. High-Quality Manganese-Doped ZnSe Nanocrystals. Nano Lett. 2001, 1, 3–7.
(10) Archer, P. I.; Santangelo, S. A.; Gamelin, D. R. Direct Observation of spin–d Exchange Interactions in Colloidal Mn2+ and Co2+ Doped CdSe Quantum Dots. Nano Lett. 2007, 7, 1037–1043.
(11) Bussian, D. A.; Crooker, S. A.; Yin, M.; Brynda, M.; Efros, Al. L.; Klimov, V. I. Tunable Magnetic Exchange Interactions in Manganese-Doped Inverted Core-Shell ZnSe-CdSe Nanocrystals. Nat. Mater. 2009, 8, 35–40.
(12) Pinchetti, V.; Di, Q.; Lorenzon, M.; Camellini, A.; Fasoli, M.; Zavelani-Rossi, M.; Meinardi, F.; Zhang, J.; Crooker, S. A.; Brovelli, S. Excitonic Pathway to Photoinduced Magnetism in Colloidal Nano-crystals with Nonmagnetic Dopants. Nat. Nanotechnol. 2018, 13, 145–151.
(13) Beaulac, R.; Archer, P. I.; Liu, X.; Lee, S.; Salley, G. M.; Dobrowolska, M.; Furdyna, J. K.; Gamelin, D. R. Spin-Polarizable Excitonic Luminescence in Colloidal Mn2+ Doped CdSe Quantum Dots. Nano Lett. 2008, 8, 1197–1201.
(14) Long, G.; Barman, B.; Delikanli, S.; Tsang Tsai, Y.; Zhang, P.; Petrou, A.; Zeng, H. Carrier-Dopant Exchange Interactions in Mn-Doped PbS Colloidal Quantum Dots. Appl. Phys. Lett. 2012, 101, No. 062410.
(15) Turyanska, L.; Hill, R. J. A.; Makarovský, O.; Moro, F.; Knott, A. N.; Larkin, O. J.; Panaté, A.; Meaney, A.; Christianen, P. C. M.; Fay, M. W.; Curly, R. J. Tuneable Paramagnetic Susceptibility and Exciton g-Factor in Mn-Doped PbS Colloidal Nanocrystals. Nanoscale 2014, 6, 8919–8925.
(16) Delikanli, S.; Akgel, M. Z.; Murphy, J. R.; Barman, B.; Tsai, Y.; Scrase, T.; Zhang, A.; Bozok, B.; Fernández-Martínez, P. L.; Christodoulides, J.; Cartwright, A. N.; Petrou, A.; Demir, H. V. Mn2+-Doped CdSe/CdS Core/Multishell Colloidal Quantum Wells Enabling Tunable Carrier-Dopant Exchange Interactions. ACS Nano 2015, 9, 12473–12479.
(17) Murphy, J. R.; Delikanli, S.; Scrase, T.; Zhang, P.; Norden, T.; Thomay, T.; Cartwright, A. N.; Demir, H. V.; Petrou, A. Time-Resolved

Notes

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Photoluminescence Study of CdSe/CdMnS/CdSe Core-Multi-SHELL Nanoplatelets. Appl. Phys. Lett. 2016, 108, 242406.

(18) Najafi, A.; Tarasek, S.; Delikanli, S.; Zhang, P.; Norden, T.; Shedre, S.; Sharma, M.; Bhattacharya, A.; Taghipour, N.; Pientka, J.; Demir, H. V.; Petrov, A.; Thomay, T. CdSe/CdMnS Nanoplatelets with Bilayer Core and Magnetically Doped Shell Exhibit Switchable Excitonic Circular Polarization: Implications for Lasers and Light-Emitting Diodes. ACS Appl. Nano Mater. 2020, 3, 3151–3165.

(19) Strassberg, B.; Delikanli, S.; Barak, Y.; Dehnel, J.; Kostadinov, A.; Maikov, G.; Hernandez-Martinez, P. L.; Sharma, M.; Demir, H. V.; Lifshitz, E. Persuasive Evidence for Electron-Nuclear Coupling in Doped Magnetic Colloidal Nanoplatelets Using Optically Detected Magnetic Resonance Spectroscopy. J. Phys. Chem. Lett. 2019, 10, 4437–4447.

(20) Beaulac, R.; Schneider, L.; Archer, P. I.; Bacher, G.; Gamelin, D. R. Light-Induced Spontaneous Magnetization in Doped Colloidal Quantum Dots. Science 2009, 325, 973–976.

(21) Rice, W. D.; Liu, W.; Pinchetti, V.; Yakovlev, D. R.; Klimov, V. I.; Crooker, S. A. Direct Measurements of Magnetic Polarons in Cd$_{1-x}$Mn$_x$Te Nanocrystals from Resonant Photoluminescence. Nano Lett. 2017, 17, 3068–3075.

(22) Lorens, S.; Ericsson, C. S.; Riesner, M.; Gamelin, D. R.; Finnblad, R.; Bacher, G. Directed Exciton Magnetic Polaron Formation in a Single Colloidal Mn$^{2+}$-CdSe/CdS Quantum Dot. Nano Lett. 2020, 20, 1896–1906.

(23) Rice, W. D.; Liu, W.; Baker, T. A.; Sinitsyn, N. A.; Klimov, V. I.; Crooker, S. A. Revealing Giant Internal Magnetic Fields Due to Spin Fluctuations in Magnetically Doped Colloidal Nanocrystals. Nat. Nanotechnol. 2016, 11, 137–142.

(24) Ithurria, S.; Dubertret, B. Quasi 2D Colloidal CdSe Platelets with Thickness Controls at the Atomic Level. J. Am. Chem. Soc. 2008, 130, 16504–16505.

(25) Furdyna, J. K.; Lee, S.; Dobrowolska, M.; Wojtowicz, T.; Liu, X. Band-Offset Engineering in Magnetic/Magnetic-Nanosemiconductor Quantum Structures. In Introduction to the Physics of Diluted Magnetic Semiconductors; Kossut, J., Gaj, J. A., Eds.; Springer Series in Materials Science; Springer Verlag: Berlin, Heidelberg, 2010; pp 103–160.

(26) Muckle, F.; Delikanli, S.; Hernandez-Martinez, P. L.; Priesner, T.; Lorenz, S.; Ackermann, J.; Sharma, M.; Demir, H. V.; Bacher, G. sp-d Exchange Interactions in Wave Function Engineered Colloidal CdSe/Mn$^{2+}$CdS Hetero-Nanoplatelets. Nano Lett. 2018, 18, 2047–2053.

(27) Zhang, P.; Norden, T.; Pientka, J. M.; Oszwałdowski, R.; Najafi, A.; Barman, B.; Tsai, Y.; Fan, W.-C.; Chou, Wu-C.; Han, J. E.; Żułtić, I.; McCombe, B. D.; Petrov, A. Optical Control of Hole Wavefunction in Type-II Magnetic Quantum Dot Structures. J. Phys. Chem. C 2019, 123, 25934–25940.

(28) Davis, A. H.; Hofman, E.; Chen, K.; Li, Z.; Khammang, A.; Zamani, H.; Franck, J. M.; Maye, M. M.; Meulenberg, R. W.; Zheng, W. Exciton Energy Shifts and Tunable Dopant Emission in Manganese-Doped Two-Dimensional CdSe/ZnS Core/Shell Nanoplatelets. Chem. Mater. 2019, 31, 2516–2523.

(29) Delikanli, S.; Yu, G.; Yeltik, A.; Bose, S.; Erdem, T.; Yu, J.; Erdem, O.; Sharma, M.; Sharma, V. K.; Quliyeva, U.; Shedre, S.; Dang, C.; Zhang, D. H.; Sum, T. C.; Fan, W.; Demir, H. V. Ultrathin Highly Luminescent Two-Monomer Colloidal CdSe Nanoplatelets. Adv. Funct. Mater. 2019, 29, 1901028.

(30) Shedre, S.; Delikanli, S.; Li, M.; Dede, D.; Pan, Z.; Han, S. T.; Fu, Y. H.; Hernández Martinez, P. L.; Yu, J.; Erdem, O.; Kuznetsov, A. I.; Dang, C.; Sum, T. C.; Demir, H. V. Ultrahigh-Efficiency Aqueous Flat Nanocrystals of CdSe/CdS@Cd$_{1-x}$Zn$_x$S Colloidal Core/Crown@Alloyed-Shell Quantum Wells. Nanoscale 2019, 11, 301–310.

(31) Adachi, S. Handbook on Physical Properties of Semiconductors; Springer US: Boston, MA, 2004.

(32) Javut, C.; Mahler, B.; Dubertret, B.; Shabaev, A.; Rodina, A. V.; Efros, A. L.; Yakovlev, D. R.; Liu, F.; Bayer, M.; Camps, G.; Biadala, L.; Bull, S.; Quelin, X.; Hermier, J.-P. Thermal Activation of Non-Radiative Auger Recombination in Charged Colloidal Nanocrystals. Nat. Nanotechnol. 2013, 8, 206–212.
Metal Nanocrystals: Synthesis and Electronic and Optical Properties; Klimov, V. I., Ed.; Dekker: New York, 2003; pp 103–141.

(48) Brumberg, A.; Harvey, S. M.; Philbin, J. P.; Diroll, B. T.; Lee, B.; Crooker, S. A.; Wasielewski, M. R.; Rabani, E.; Schaller, R. D. Determination of the In-Plane Exciton Radius in 2D CdSe Nanoplatelets via Magneto-Optical Spectroscopy. ACS Nano 2019, 13, 8589–8596.

(49) Ivanov, V. Yu; Godlewski, M.; Yakovlev, D. R.; Ryabchenko, S. M.; Karczewski, G.; Waag, A. Time-Resolved Optically-Detected Magnetic Resonance of II-VI Diluted Magnetic-Semiconductor Heterostructures. Phys. Status Solidi A 2007, 204, 174–178.

(50) Ivanov, V. Yu; Godlewski, M.; Yakovlev, D. R.; Kneip, M. K.; Bayer, M.; Ryabchenko, S. M.; Waag, A. Optically Detected Magnetic Resonance in (Zn,Mn)Se/(Zn,Be)Se Quantum Wells. Phys. Rev. B: Condens. Matter Mater. Phys. 2008, 78, No. 085322.

(51) Matarrese, L.M.; Kikuchi, C. Paramagnetic Resonance Absorption of Mn^{2+} in Single Crystals of Zincblende. J. Phys. Chem. Solids 1956, 1, 117–127.

(52) Lambe, J.; Kikuchi, C. Paramagnetic Resonance of CdTe:Mn and CdS:Mn. Phys. Rev. 1960, 119, 1256–1260.

(53) Heiman, D.; Wolff, P. A.; Warnock, J. Spin-Flip Raman Scattering, Bound Magnetic Polaron, and Fluctuations in (Cd,Mn)Se. Phys. Rev. B: Condens. Matter Mater. Phys. 1983, 27, 4848–4860.

(54) Stühler, J.; Schaack, G.; Dahl, M.; Waag, A.; Landwehr, G.; Kavokin, K. V.; Merkulov, I. A. Multiple Mn^{2+}-Spin-Flip Raman Scattering at High Fields via Magnetic Polaron States in Semimagnetic Quantum Wells. Phys. Rev. Lett. 1995, 74, 2567–2570.

(55) Bao, J. M.; Bragas, A. V.; Furdyna, J. K.; Merlin, R. Control of Spin Dynamics with Laser Pulses: Generation of Entangled States of Donor-Bound Electrons in a Cd_{1−x}Mn_x Te Quantum Well. Phys. Rev. B: Condens. Matter Mater. Phys. 2005, 71, No. 045314.

(56) Smith, L. C.; Davies, J. J.; Wolverson, D.; Lentze, M.; Geurts, J.; Wojtowicz, T.; Karczewski, G. Dependence of Multiple Mn^{2+} Spin-Flip Raman Scattering in Quantum Wells on the Magnetic Field Direction. Phys. Rev. B: Condens. Matter Mater. Phys. 2008, 77, 115341.

(57) Kudlacik, D.; Sapega, V. F.; Yakovlev, D. R.; Kalitukha, I. V.; Shornikova, E. V.; Rodina, A. V.; Ivchenko, E. L.; Dimitriev, G. S.; Nasilowski, M.; Dubertret, B.; Bayer, M. Single and Double Electron Spin-Flip Raman Scattering in CdSe Colloidal Nanoplatelets. Nano Lett. 2020, 20, 517–525.

(58) Feng, D.; Yakovlev, D. R.; Dubertret, B.; Bayer, M. Charge Separation Dynamics in CdSe/CdS Core/Shell Nanoplatelets Addressed by Coherent Electron Spin Precession. ACS Nano 2020, 14, 7237–7244.

(59) Kavokin, K. V.; Merkulov, I. A. Multispin Raman Paramagnetic Resonance: Quantum Dynamics of Classically Large Angular Momenta. Phys. Rev. B: Condens. Matter Mater. Phys. 1997, 55, R7371–R7374.