Electronic transport in ferromagnetic alloys and the Slater-Pauling Curve

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Experimental measurements of the residual resistivity \( \rho(x) \) of the binary alloy system Fe\(_{1-x}\)Cr\(_{x}\) have shown an anomalous concentration dependence which deviates significantly from Nordheim’s rule. In the low \( x < 10\% \) Cr concentration regime the resistivity has been found to increase linearly with \( x \) until \( 10\% \) Cr where the resistivity reaches a plateau persisting to \( 20\% \) Cr. In this paper we present \textit{ab-initio} calculations of \( \rho(x) \) which explain this anomalous behavior and which are based on the Korringa-Kohn-Rostoker (KKR) method in conjunction with the Kubo-Greenwood formalism. Furthermore we are able to show that the effects of short-range ordering or clustering have little effect via our use of the nonlocal coherent-potential approximation (NL-CPA). For the interpretation of the results we study the alloys’ electronic structure by calculating the Bloch spectral function particularly in the vicinity of the Fermi energy. From the analysis of our results we infer that a similar behavior of the resistivity should also be obtained for iron-rich Fe\(_{1-x}\)V\(_{x}\) alloys – an inference confirmed by further explicit resistivity calculations. Both of these alloy systems belong to the same branch of the famous Slater-Pauling plot and we postulate that other alloy systems from this branch should show a similar behavior. Our calculations show that the appearance of the plateau in the resistivity can be attributed to the dominant contribution of minority spin electrons to the conductivity which is nearly unaffected by increase in \( \text{Cr/V} \) concentration \( x \) and we remark that this minority spin electron feature is also responsible for the simple linear variation of the average moment in the Slater-Pauling plot for these materials.

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I. INTRODUCTION

The Slater-Pauling plot of average magnetisation per atom \( M \) versus valence electron number \( N_v \) plays a pivotal role in the understanding of the properties of ferromagnetic alloys.\(^1\) Its triangular structure of two straight lines with gradients of opposite sign neatly categorises most alloys into one of two classes where \( \frac{dM}{dN_v} \pm 1 \). Long ago Mott\(^2\) pointed out how this behavior can be explained by requiring either the number of majority or minority spin electrons to be fixed. This notion has subsequently been confirmed and given substance by modern spin density functional theory (DFT) calculations\(^3\). In this paper we follow the implications of this for the residual resistivities of ferromagnetic alloys. In particular, using the latest \textit{ab-initio} techniques for describing disordered systems, we demonstrate how the measured apparently anomalous resistivities of iron-rich Fe\(_{1-x}\)Cr\(_{x}\) alloys\(^4\) are directly attributable to their average minority-spin electron number being fixed and consequently their location on the \( \frac{dM}{dN_v} = +1 \) section of the Slater-Pauling plot. We postulate that other alloys in this category should also show the same behavior and we strengthen this conjecture by the findings from another detailed \textit{ab-initio} study of Fe\(_{1-x}\)V\(_{x}\) alloys. We also infer that short-range order should have little effect on the resistivities of alloys in this category and again we are able to back up these remarks by detailed specific \textit{ab-initio} calculations.

Many DFT calculations for disordered ferromagnetic alloys show that the majority-spin electrons ‘see’ little disorder and that the majority-spin \( d \) states are fully occupied. This leads to \( \frac{dM}{dN_v} = -1 \). In contrast the minority-spin electron states are significantly affected by disorder. The overall electronic transport is therefore taken up by the \( sp \)-majority-spin electrons. Alloys in this category include fcc-based CoMn, FePt and Ni-rich NiFe alloys.

On the other hand, for some other alloys, typically Fe-rich, bcc-based alloys and many Heusler alloys, the number of minority-spin \( d \) electrons is fixed as the Fermi energy \( E_F \) is pinned at a low level in a trough of the \( d \) electron density of states. \( \frac{dM}{dN_v} = +1 \) of the Slater-Pauling curve follows directly from this\(^5\). It is the ramifications of this feature for the electronic transport in such alloys that we investigate here. This time disorder is ‘seen’ strongly by the majority-spin electrons and rather weakly by the minority-spin electrons. Fig. 1 provides a relevant illustration for a bcc Fe\(_{0.8}\)Cr\(_{0.2}\) disordered alloy\(^6\). The Fe- and Cr-related minority-spin densities of states have similar structure in contrast to those of majority spin. \( E_F \) is positioned in a valley making the average number of minority spin electrons \( \approx 3 \). Moreover from these observations we can expect the resistivity to be dominated by minority spin electrons and to be rather insensitive to overall composition and short-range order. Recently, measurements of the residual electrical resistivity of iron-rich Fe\(_{1-x}\)Cr\(_{x}\) alloys have been reported and described as anomalous. The measurements show that the resistivity increases as small amounts of Cr are added to Fe until a plateau is reached ranging from \( x = 10\% \) to...
20%. This behavior differs markedly from the Nordheim parabolic concentration dependence. An analysis of the data is hindered by a complexity of short-range order in Fe$_{1-x}$Cr$_x$. Mirebeau et al. reported that for $x < 10\%$ the system develops short-ranged order whereas for larger $x$ short-ranged clustering is found. At higher Cr concentrations still ($> 20\%$), the alloys can undergo on aging a separation into Fe-rich ($\alpha$) and Cr-rich ($\alpha'$) phases, leading either to a miscibility gap or a transformation into a tetragonal $\sigma$ phase.

We use the Kubo-Greenwood formalism implemented with the Kopp-Kohn-Rostoker (KKR) method for ab-initio calculations of the residual resistivities of Fe$_{1-x}$Cr$_x$ alloys. Disorder is accounted for by the use of the coherent potential approximation (CPA). In order to examine the effects of short-ranged order within the disorder we use our recently developed method which involves the non-local CPA (NL-CPA). We complement our ab-initio resistivity calculations with Bloch spectral function calculations which show the electronic structure in the vicinity of $E_F$ and enable a connection to be made to the semi-classical Boltzmann description of electronic transport properties.

We find that our calculations fully support our initial expectations outlined above which are linked to the alloys' location on the Slater-Pauling plot in addition to describing the experimental data well. Moreover from further calculations for Fe$_{1-x}$V$_x$ alloys we predict that a similar behavior will be found for these materials as well as for other systems sited in this region of the Slater-Pauling plot.

The next section outlines the ab-initio theoretical framework (full details are given in Refs. 14 and 15). This is followed by our study of the resistivity of Fe$_{1-x}$Cr$_x$ as a function of $x$ together with Bloch spectral function interpretation. We then describe a similar investigation of Fe$_{1-x}$V$_x$ alloys. The last section summarises and emphasises the overall conclusions.

## II. Theory

### A. Kubo-Greenwood equation

The basis of our investigations is supplied by the Kubo-Greenwood equation for the symmetric part of the conductivity tensor:

$$\sigma_{\mu\nu} = \frac{\hbar}{\pi N \Omega} \text{Tr} \langle \hat{j}_\mu \mathcal{G}^+(E_F) \hat{j}_\nu \mathcal{G}^+(E_F) \rangle. \quad (1)$$

Here $N$ is the number of atomic sites, $\Omega$ the volume per atom, $\text{Tr}$ indicates an averaging over configurations and $\mathcal{G}^+(E_F)$ is the imaginary part of the retarded one particle Green function at the Fermi energy $E_F$. For the determination of $\mathcal{G}^+(E_F)$ we use multiple scattering theory (MST) which is the basis of the KKR band structure method. Within MST the real space representation of $\mathcal{G}^+$ has the following form:

$$\mathcal{G}^+(\vec{r}, \vec{r}', E) = \mathcal{Z} \sum_{\Lambda_1, \Lambda_2} Z_{\Lambda_1}(\vec{r}, E) \tau_{\Lambda_1, \Lambda_2}(E) Z_{\Lambda_2}^\ast(\vec{r}', E). \quad (2)$$

Using a fully relativistic implementation, the wave functions $Z(Z^\ast)$ are the regular right (left) hand side solutions of the Dirac equation, $\tau$ is the scattering path operator and $\Lambda = (\kappa, \mu)$ with $\kappa$ and $\mu$ being the relativistic spin-orbit and magnetic quantum numbers. Finally, $\hat{j}_\mu$ in Eq. (1) is the current density operator that is given in relativistic form by

$$\hat{j}_\mu = ee \alpha_\mu \tau_\mu. \quad (3)$$

where $\alpha_\mu$ is one of the standard Dirac matrices. The central step to calculate the conductivity is to handle the averaging over all possible configurations. For a randomly disordered system the CPA is a well established method for the configuration averaging. The CPA introduces an effective medium which represents the electronic properties of the disordered alloy. This effective medium is described by its single site $t$ matrix $t_{\text{CPA}}$ in combination with its averaged scattering path operator $\Sigma_{\text{CPA}}$

$$\Sigma_{\text{CPA}} = \frac{1}{\Omega_{\text{BZ}}} \int_{\Omega_{\text{BZ}}} \frac{d^3k}{(2\pi)^3} \left[ \mathcal{U}_{\text{CPA}}^{-1} - \mathcal{G}(\vec{k}, E) \right]^{-1} \quad (4)$$

where the underline indicates matrices with respect to the spin-angular character $\Lambda$. Assuming a binary alloy $A_{1-x}B_x$, $\Sigma_{\text{CPA}}$ and $t_{\text{CPA}}$ have to fulfill the CPA condition

$$\Sigma_{\text{CPA}} = (1 - x) \Sigma_A + x \Sigma_B. \quad (5)$$

$\Sigma_{\Lambda(B)}$ is the scattering path operator for an atom of type $A(B)$ embedded into the CPA medium and $\mathcal{G}(\vec{k}, E)$ is
the KKR structure constants matrix. With these CPA equations it is possible to construct the effective medium iteratively. Butler derived within the CPA a scheme to handle the averaging over configurations of two Green functions. His formulation of the Kubo-Greenwood equation on the basis of the KKR-CPA is widely applied and gives in general good agreement with experimental data.

It has to be emphasized that the CPA is a single site theory and therefore neglects correlations concerning the occupation of the neighboring atomic sites. For that reason one has to use more elaborate methods to include SRO effects. One possibility is to use the NL-CPA. The NL-CPA creates (as the CPA) an effective medium, and can be understood as a cluster generalization of the well established CPA. The corresponding NL-CPA equations can be written as:

\[
\Omega^{\gamma}_{\text{NLCPA}} = \frac{1}{\Omega_{\text{BZ}}} \sum_{\vec{K}_n} \left( \int_{\Omega_{\vec{K}_n}} d^3k \left[ (\Omega^{\text{NL-CPA}})^{-1} - \Omega^{\gamma}(\vec{k}, E) \right] - \delta \Omega^{\gamma}(\vec{K}_n, E) \right)^{-1} e^{i \vec{K}_n \cdot (\vec{r}_1 - \vec{r}_2)}
\]

(6)

\[
\Omega^{\gamma}_{\text{NLCPA}} = \sum_{\gamma} P_{\gamma} \Omega^{\gamma}_n \quad (\text{with } \sum_{\gamma} P_{\gamma} = 1),
\]

(7)

B. Bloch spectral functions

In a most general way the density of states may be defined as:

\[
n(E) = \sum_{n} \delta(E - E_n),
\]

(9)

where \(E_n\) are the electronic eigenvalues of the system. In analogy the Bloch spectral function (BSF) can be defined by:

\[
A(E, \vec{k}) = \sum_{n} \delta[E - E_n(\vec{k})]
\]

(10)

and for that reason can be regarded as a \(\vec{k}\)-resolved density of state. Dealing with an ordered system and a given \(\vec{k}\)-vector the BSF has at the positions of the eigenvalues an infinitely sharp peak and everywhere else it is zero. If one has an alloy instead of a perfect crystal an appropriate expression for the BSF within KKR-CPA was worked out by Faulkner and Stocks.

The matrices \(F^c\) and \(F^{cc}\) are given in terms of the overlap integrals

\[
F^{\alpha\beta}_{\Lambda\Lambda'} = \int_{\Omega} d^3r Z_\Lambda^\alpha(E, r) Z_{\Lambda'}^{\beta}(E, r). \tag{13}
\]

(13)

\(\alpha, \beta\) denotes an atom type of the alloy. For more details and explicit expressions see Ref.\textsuperscript{17}. Compared to a pure system, the BSF for an alloy becomes broadened due to the disorder. This broadening can be related to the lifetime of an electron in a Bloch state and is therefore quite useful for the interpretation of resistivity data\textsuperscript{16}. With the BSF it is possible to discuss a dispersion relation \(E(\vec{k})\) even for alloys. Strictly spoken such a dispersion relation is in general not defined for alloys because \(\vec{k}\) is not a good quantum number for disordered systems. Nevertheless, the dispersion relation represented by the BSF can be used to calculate Fermi velocities\textsuperscript{16} and gives therefore useful hints for the interpretation of resistivity data.

C. Computational details

All calculations were done in the framework of spin density functional theory using the local spin density approximation (LSDA) with the parameterization of Vosko.
et al.\textsuperscript{33} for the exchange correlation potential. The CPA and the NL-CPA formulations of the Kubo-Greenwood equation were implemented within the self-consistent, spin polarized, relativistic KKR (SPR-KKR) scheme\textsuperscript{34}. All calculations include vertex corrections\textsuperscript{14,15}. To ensure convergence of the results with respect to the angular momentum expansion the cutoff $l_{\text{max}} = 4$ has been used.

III. RESULTS

A. CPA Results

The central result of our calculations is shown in Fig. 2. This figure shows the residual resistivity of Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$ as a function of the Cr/V concentration $x$. As mentioned above, the experimental Fe$_{1-x}$Cr$_x$ data show an anomalous behavior. In the low Cr concentration regime ($\approx 10\%$) the residual resistivity increases with increasing Cr concentration. Further increase of the Cr content does not lead to a further increase of the resistivity. Our theoretical results show the same variation with the Cr concentration. At 10\% Cr we obtain the highest value for the resistivity. If one further increases the Cr concentration, the resistivity stays more or less constant at $\approx 8\mu \Omega \text{cm}$.

The Fe$_{1-x}$V$_x$ alloys show a similar behavior for the theoretical residual resistivity. With increasing V concentration the residual resistivity increases up to $\approx 2\mu \Omega \text{cm}$ (at 6\% V). Further increase of the V concentration leads only to small changes in the residual resistivity. This behavior can be explained by a different variation of the electronic structure for the majority and minority spin subsystems when the Cr/V concentration changes. Adding Cr to pure Fe in a random way the disorder in the system increases and with this the resistivity increases. This conventional behavior is observed in the regime with a Cr content smaller than $\approx 8\%$ Cr where the system shows a Nordheim like behavior. To identify the contribution of the majority/minority spin subsystems to the conductivity, we calculated the BSF according to Eq. (11). Fig. 3 shows the total and spin projected BSF for three different Cr concentrations (4\%, 12\% and 20\% Cr). The black regions correspond to values $> 50$ a.u.. For a better resolution the cusps of the BSF have been cut.

FIG. 2: (Color online) The residual resistivity of Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$ as a function of the Cr/V concentration $x$. The asterisks (red line) show the experimental data for Fe$_{1-x}$Cr$_x$ of Ref. 7 at 4.2K. The triangles and diamonds (black lines) show our CPA results for Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$, respectively.

FIG. 3: Total and spin projected BSF of Fe$_{1-x}$Cr$_x$ at the Fermi energy in the (001) plane for different Cr concentrations (top: 4\% Cr, middle: 12\% Cr, bottom: 20\% Cr). The black regions correspond to values $> 50$ a.u.. For a better resolution the cusps of the BSF have been cut.
FIG. 4: BSF along the Γ - X direction for the minority spin subsystem in Fe$_{1-x}$Cr$_x$ for three different Cr concentrations (4%, 12% and 20% Cr). The cusps of the BSF have been cut at 300 a.u..

FIG. 5: (Color online) Spin resolved conductivities $\sigma_\uparrow$ and $\sigma_\downarrow$ for Fe$_{1-x}$Cr$_x$.

present to the right of the split peak. This peak is due to a hybridisation with the majority subsystem. This can be inferred from Fig. 4 if one compares the minority and majority BSF for 4% Cr. The reason for this hybridisation is, that in fully relativistic calculations the spin is not a good quantum number because of the presence of spin-orbit coupling.$^{35}$

The behavior of the three remaining peaks is quite different. The narrow peak shifts with increasing Cr concentration towards the Γ-point and at 20% Cr this peak overlaps with the peak closest to the Γ-point. The split peak remains nearly fixed at its position but one observes a narrowing with increasing Cr concentration, which corresponds to an increased lifetime of this state.

For comparison we also calculated BSF for Fe$_{1-x}$V$_x$ and found a similar behavior of the majority/minority spin subsystem as for Fe$_{1-x}$Cr$_x$. Fig. 6 shows the spin projected BSF for Fe$_{0.8}$V$_{0.2}$. One can see that again the majority component becomes smeared out whereas the minority component displays sharp peaks. To get a more detailed picture of the Fe$_{1-x}$V$_x$ BSF we show in Fig. 6 a similar picture as shown in Fig. 4 for Fe$_{1-x}$Cr$_x$. If one compares Fig. 7 with Fig. 4 one can see that for Fe$_{1-x}$V$_x$ the BSF peaks are more sharp than for Fe$_{1-x}$Cr$_x$. Therefore one can say that the minority spin electrons “see” a smaller difference between Fe and V atoms compared to Fe and Cr atoms. This explains why the residual resistivities are higher in Fe$_{1-x}$Cr$_x$ compared to Fe$_{1-x}$V$_x$. Fig. 7 shows that the increased disorder due to the increased V concentration do not affect the BSF peaks of the minority spin subsystem.

To identify the character of the smeared out states from the majority subsystem, we projected the Fe$_{1-x}$Cr$_x$ BSF according to its s-, p- and d-contributions. This is shown in Fig. 8. The main part of the majority states has d-like character. These states obviously strongly broaden with increasing Cr concentration. This behavior is opposite to that of the minority subsystem although this is also dominated by d-like states. The different behavior of the d-states for the two spin subsystems can also be seen in...
The density of states. In Figs. 1 and 9 the spin projected DOS of Fe$_{1-x}$Cr$_x$ for two different Cr concentrations is shown. In addition to the total DOS we show the d-like part of the DOS. The DOS shown in Fig. 1 is very close to that of pure Fe. One can see that for the majority component also the antibonding Fe d-states are occupied whereas for the minority component the Fermi level is located in a so-called pseudogap below the antibonding states. Fig. 1 clearly shows the relative positions of the Cr and Fe d-states. These states are strongly hybridized for the minority component. The opposite happens in the majority spin channel, where the Fe and the Cr d-states are well separated in energy.

With increasing Cr concentration the antibonding Fe d-peak of the majority component becomes more and more depopulated and new states appear above the Fermi level. Olsson et al.\textsuperscript{11} showed that this leads to a completely smeared out band at approximately equiatomic composition. If one compares this with the behavior of the d-states of the minority component, one can see that the increase in Cr concentration has no effect on the total DOS of the minority component.

It is well known that the DOS of Fe$_{1-x}$V$_x$ consists of a minority spin subsystem where the Fermi energy is pinned in a pseudogap and a majority spin subsystem which becomes broadened and depopulated with increasing V concentration\textsuperscript{44}. These similar characteristics of the Fe$_{1-x}$Cr$_x$ and the Fe$_{1-x}$V$_x$ DOS are responsible for the appearance of the Slater-Pauling curve for the magnetic moment of these alloys. Due to the fact that the number of minority electrons ($N_{d\downarrow}$) is independent of the Cr/V concentration the magnetization per atom $M$ varies linearly with the Cr/V concentration\textsuperscript{2}

$$ M = Z - 2N_{d\downarrow} - 2N_{sp\downarrow}, $$

with $Z$ the number of valence electrons. The number of sp-electrons in the minority spin system $N_{sp\downarrow}$ changes only very little across the 3d row\textsuperscript{44}. Therefore one can conclude that the Cr/V concentration independent hybridized Fe and Cr/V d-states of the minority spin subsystem are responsible for the appearance of the Slater-Pauling curve and in addition for the apparently anomalous behavior of the residual resistivity of these materials.

The discussion of the electronic structure of Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$ in terms of the BSF and DOS curves has obviously been made in the spirit of the two-current model for the conductivity of spin-polarized solids. The fully relativistic approach for calculating the conductivity used here strictly speaking doesn’t allow a decomposition of the conductivity into spin channels. The reason for this is that spin-orbit coupling not only gives rise to the off-diagonal elements $\sigma_{xy}$ mentioned above but also to spin-flip contributions that influence the isotropic conductivity or resistivity, respectively. If the spin-orbit coupling strength is not too strong, however, an approximate decomposition can nevertheless be made. As was demonstrated in Ref. 36, ignoring the small spin-flip elements connected with the current density operator in Eq. (3), one can still define a spin-projected conductivity. This is indeed justified for Fe$_{1-x}$Cr$_x$ by the fact that the sum of the approximate conductivities $\sigma_1 + \sigma_1$ hardly differs from the conductivity calculated in a relativistic way (Fig. 2). The results for $\sigma_1$ and $\sigma_1$ shown in Fig. 3 indeed confirm the picture that evolved from the BSF; i.e. $\sigma_1$ is about two orders of magnitude larger than $\sigma_1$ and is nearly concentration independent for $x > 8\%$. As a consequence the resistivity is dominated by the majority spin channel.

In summary the resistivity increase from 0-10% Cr (0-6% V) is due to the increased disorder scattering for the majority spin subsystem; roughly speaking, the contribution of the majority subsystem to the conductivity drops down. This drop down can be explained by a smeared out BSF for this component. At higher Cr/V concentrations only the minority subsystem contributes to the conductivity. The increase of the Cr/V concentration leads to no broadening of the minority states. Therefore,
the contribution of this component to the conductivity in the range of 10-20% Cr (6-20% V) is constant. This leads to a nearly constant resistivity in that concentration regime.

**B. NL-CPA Results**

The next step in our analysis is to investigate the influence of SRO effects on the residual resistivity as this was suggested to be the reason for the anomalous concentration dependence of the residual resistivity. To include SRO effects we use the NL-CPA which is, as explained above, a cluster generalization of the CPA. Therefore we have to define appropriate cluster configurations and their associated probabilities \( P_x \). We used the smallest possible bcc cluster with two atoms. This leads to four different cluster configurations e.g. \( \text{Fe}_{1-x}\text{Cr}_x \): pure Fe (FeFe), pure Cr (CrCr) and two mixed clusters with different occupation of the lattice sites (FeCr, CrFe). The probabilities of the configurations depend on the investigated ordering case. For example in the case of \( \text{Fe}_{0.5}\text{Cr}_{0.5} \) and SRO only the configurations FeCr and CrFe have to be considered. For the simulation of clustering effects only the pure configurations FeFe and CrCr have non-zero probabilities and to simulate total disorder all configurations are used. In Ref. 15 a detailed description how to define the configuration probabilities for a bcc lattice is given. To display the contribution of the different cluster configurations to the density of states of a disordered \( \text{Fe}_{1-x}\text{Cr}_x \) crystal we show in Fig. 10 the cluster resolved density of states for two different Cr concentrations. From this figure one can see that the total DOS agrees very well with the total CPA DOS from Figs. 1 and 9. The solid (black) line shows the total DOS, the dashed (red) line shows the contribution of the FeFe-cluster, the (blue) dotted line of the FeCr-cluster, the (green) dashed-dotted-dotted line of the CrFe-cluster and the (orange) dashed-dotted-dotted line of the CrCr-cluster.

**FIG. 10**: (Color online) Cluster resolved NL-CPA density of states of disordered \( \text{Fe}_{1-x}\text{Cr}_x \) (top: 4% Cr, bottom: 20% Cr). The solid (black) line shows the total DOS, the dashed (red) line shows the contribution of the FeFe-cluster, the (blue) dotted line of the FeCr-cluster, the (green) dashed-dotted-dotted line of the CrFe-cluster and the (orange) dashed-dotted-dotted line of the CrCr-cluster.

The influence of ordering effects (SRO and clustering) on the residual resistivity is very small for these systems. In Ref. 15 the same formalism was applied to bcc CuZn and gave a strong variation of the resistivity as function of the ordering state. The small influence of ordering effects on the resistivity for \( \text{Fe}_{1-x}\text{Cr}_x \) was also found experimentally by Mirebeau et al.2. This shows that the formalism from Ref. 15 can handle various different ordering dependences of the residual resistivity.

**IV. DISCUSSION AND SUMMARY**

The present work deals on an *ab-initio* level with the anomalous concentration dependence of the residual re-
The resistivity of Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$ as function of the concentration $x$. Fe$_{1-x}$Cr$_x$: The asterisks (red line) show the experimental data of Ref. 7 and the triangles (black line) show our CPA results. The circles (yellow line) show the NL-CPA results for the disordered alloys, the diamonds (green line) show results when SRO is included and the squares (blue line) when short-range clustering is included. Fe$_{1-x}$V$_x$: The diamonds (black line) show our CPA results and the crosses (magenta line) show results when SRO is included.

In addition, we investigated the influence of short-ranged correlations in the lattice site occupation by employing the NL-CPA formulation of the Kubo-Greenwood equation. The inclusion of such short-range effects has only little influence on the results. The comparison of the Fe$_{1-x}$Cr$_x$ calculations with experiment show satisfying agreement. The difference in the height of the plateau, as compared to the experiment, could be attributed to impurities, lattice defects, grain boundaries, etc. which are always present in samples and therefore contained in the experimental data. Such imperfections, which have been neglected in the present calculations, lead in general to an increase of the measured resistivity.

Our calculations show the initial linear increase albeit with a lower slope than seen in experiment. In Ref. 8 it is argued that this is a consequence of the limitations of the CPA for alloys with a dominant concentration of one constituent. However, it should be pointed out that our NL-CPA results confirm the single-site CPA data. Our calculations reveal a plateau of the residual resistivity starting at the same Cr concentration as seen in experiment (at 10% Cr). This is in variance to an earlier theoretical study which finds the starting point of the plateau only at $\approx$ 20% Cr.

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**FIG. 11:** (Color online) The resistivity of Fe$_{1-x}$Cr$_x$ and Fe$_{1-x}$V$_x$ as function of the concentration $x$. Fe$_{1-x}$Cr$_x$: The asterisks (red line) show the experimental data of Ref. 7 and the triangles (black line) show our CPA results. The circles (yellow line) show the NL-CPA results for the disordered alloys, the diamonds (green line) show results when SRO is included and the squares (blue line) when short-range clustering is included. Fe$_{1-x}$V$_x$: The diamonds (black line) show our CPA results and the crosses (magenta line) show results when SRO is included.
