Time resolution of the plastic scintillator strips with matrix photomultiplier readout for J-PET tomograph

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Abstract
Recent tests of a single module of the Jagiellonian Positron Emission Tomography system (J-PET) consisting of 30 cm long plastic scintillator strips have proven its applicability for the detection of annihilation quanta (0.511 MeV) with a coincidence resolving time (CRT) of 0.266 ns. The achieved resolution is almost by a factor of two better with respect to the current TOF-PET detectors and it can still be improved since, as it is shown in this article, the intrinsic limit of time resolution for the determination of time of the interaction of 0.511 MeV gamma quanta in plastic scintillators is much lower. As the major point of the article, a method allowing to record timestamps of several photons, at two ends of the scintillator strip, by means of matrix of silicon photomultipliers (SiPM) is introduced. As a result of simulations, conducted with the number of SiPM varying from 4

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to 42, it is shown that the improvement of timing resolution saturates with the growing number of photomultipliers, and that the $2 \times 5$ configuration at two ends allowing to read twenty timestamps, constitutes an optimal solution. The conducted simulations accounted for the emission time distribution, photon transport and absorption inside the scintillator, as well as quantum efficiency and transit time spread of photosensors, and were checked based on the experimental results. Application of the $2 \times 5$ matrix of SiPM allows for achieving the coincidence resolving time in positron emission tomography of $\approx 0.170$ ns for 15 cm axial field-of-view (AFOV) and $\approx 0.365$ ns for 100 cm AFOV. The results open perspectives for construction of a cost-effective TOF-PET scanner with significantly better TOF resolution and larger AFOV with respect to the current TOF-PET modalities.

Keywords: positron emission tomography, scintillator detectors, timing

(Some figures may appear in colour only in the online journal)

1. Introduction

There is a continued interest in improving time resolution of scintillator detectors. Such improvements are especially challenging in case of the registration of low energy gamma quanta where the time resolution is limited by the low statistics of scintillation photons.

Superior time resolution for registration of low energy gamma quanta is of crucial importance in the nuclear medicine applications as e.g. in positron emission tomography (PET), where the new generation of PET scanners utilizes for the image reconstruction differences between time of flight (TOF) of annihilation quanta from the annihilation vertex to the detectors (Moses and Derenzo 1999, Moses 2003, Humm et al 2003, Townsend et al 2004, Karp et al 2008, Conti 2009, Conti et al 2009).

In order to improve the TOF resolution and to increase a geometrical acceptance of the PET scanners we are developing a J-PET detection system (Moskal et al 2011, 2014a, Raczyński et al 2014, Moskal et al 2015, Raczyński et al 2015). The system is based on long strips of plastic scintillators which are characterized by better timing properties than the inorganic scintillator crystals used in the state of the art PET scanners (Humm et al 2003, Townsend et al 2004, Karp et al 2008, Conti 2009)

Left panel of figure 1 shows a schematic view of two detection modules of the J-PET detector, where (similarly as described in the Nickles and Meyer (1978)) the time of the interaction (hit-time) of gamma quantum in the scintillator ($t_{hit} = (t^L + t^R)/2$) is calculated as an arithmetic mean of times at left ($t^L$) and right ($t^R$) side of the strip. The position of interaction along the strip (axial hit position) may be in the first approximation calculated as $\Delta z = (t^L - t^R)v/2$, where $v$ denotes the speed of light signals in the scintillator strip. For example for plastic strips with cross section of $0.5 \text{ cm} \times 1.9 \text{ cm}$ the effective light signal velocity is equal to $v = 12.2 \text{ cm ns}^{-1}$ (Moskal et al 2014a). Thus, in the case of strips with the length of 30 cm characterized with the hit-time resolution of 0.188 ns (FWHM) the axial position resolution amounts to about 2.3 cm (FWHM) (Moskal et al 2014a). The position along the line-of-response ($\Delta \text{LOR}$) between two strips (e.g. up and down shown in the left panel of figure 1) is calculated as $\Delta \text{LOR} = (t^\text{up}_{hit} - t^\text{dw}_{hit})c/2$, where $c$ denotes the speed of light. The hit-time and hence also axial position resolution may still be improved e.g. by probing photomultiplier pulses in the voltage domain by a newly developed electronics (Palka et al 2014), and by applying in the reconstruction the compressing sensing theory (Raczyński et al 2014, Raczyński et al 2015)
and the library of synchronized model signals (Moskal et al 2015). The timing resolution, as it is introduced hereafter in this article, can be also improved by making a readout allowing to record time-stamps from larger number of photons compared to the case of the vacuum tube photomultipliers.

Due to the relatively low costs of plastic scintillators and their large light attenuation length (in the order of 100 cm) it is possible to construct a detector with a long axial field-of-view in a cost effective way. This feature makes the J-PET detector competitive to the present solutions as regards the whole-body imaging. One of the possible arrangements of the scintillator strips in the J-PET scanner is visualized in the right panel of figure 1. Such alignment permits to use more than one detection layer thus increasing the efficiency of gamma quanta registration.

Plastic scintillators were not used so far as possible detectors for PET imaging due to the negligible probability of the photoelectric effect and lower detection probability with respect to the inorganic crystals. With the plastic scintillators the detection of 0.511 MeV gamma quanta is based in practice only on the Compton scattering. In figure 2 we show a distribution of Compton scattered electron energy for (i) the energy of gamma quanta reaching the detector without scattering in the patient’s body, (ii) after the scattering through an angle of 30 degrees and (iii) after scattering through an angle of 60 degrees. The presented distributions show that in order to limit registration of gamma quanta scattered in the patient to the range from 0 to about 60 degrees (as it was applied earlier e.g. in some LSO or BGO based tomographs (Humm et al 2003)), one has to use an energy threshold of about 0.2 MeV (Moskal et al 2012). The scatter fraction can be further reduced at the expense of the sensitivity, yet it should be noted that its suppression to the level achievable in the newest LSO based scanners with the energy window of 0.440–0.625 MeV (Surti et al 2007) is questionable. However, for the quantitative statement, more detailed investigations are needed. Application of 0.2 MeV threshold suppresses also to the negligible level signals due to the secondary Compton scattering in the detector material (Kowalski et al 2015). So far we have obtained 0.188 ns (FWHM)
of hit-time resolution for the registration of 0.511 MeV annihilation quanta by means of 30 cm long strips of plastic scintillators read out at both ends by vacuum tube photomultipliers (Moskal et al 2014a). The experiment was performed using a collimated beam of annihilation quanta from the $^{68}$Ge isotope placed inside a lead collimator with a 1.5 mm wide and 20 cm long slit. A dedicated mechanical system allowed us to irradiate the tested scintillator at the desired position. A coincidence registration of signals from the tested module and the reference detector on the other side of the collimator ensured selection of annihilation gamma quanta. A tested module consisted of a BC-420 plastic scintillator (Saint Gobain Crystals 2016) with dimensions of $0.5 \times 1.9 \times 30$ cm connected optically at the ends to the Hamamatsu photomultipliers R5230 (Hamamatsu 2016). The experimental setup and results of the measurements are described in detail in Moskal et al (2014a).

In principle, information about a time of interaction of gamma quantum in the scintillator is carried by all emitted scintillation photons. However, in practice in the typical detectors, only few first registered photons, contributing to the leading edge of the electrical signal generated by the photoelectric converters, are utilized in the determination of the onset of these signals and hence in the determination of the time of the gamma quantum interaction. This is also the case for the scintillator strips in the current version of the J-PET detector (see upper part of figure 3), where the time of the interaction is determined as an arithmetic mean of times at which electric signals generated by photomultipliers attached to both ends cross a preset threshold voltage. Therefore, the time resolution may be improved by making a readout allowing to record timestamps from larger number of photons arriving at the scintillator edge. There are first attempts to register all timestamps using arrays of single-photon avalanche diodes (Meijlink et al 2011), but presently the registration of arrival time of all photons with a good time resolution at large areas is still rather impractical. It is, however, important to stress that the intrinsic timing resolution limit is approached already when using only about 20 timestamps from first detected photons (Seifert et al 2012a). In this article we study the possibility of improving the time resolution for the large size detectors (few tens of centimeters) by registration of timestamps from several photons. This may be realized by preparing a readout in the form of an array with several SiPM photomultipliers as it is indicated in the lower part of figure 3. In such a case, a set of all registered photons is divided into several subgroups and a time of the registration of the first photon in each subgroup is recorded. This allows to construct estimators of the time of gamma quantum interaction based on the number of timestamps equal to the number of SiPM photomultipliers.

Figure 2. Energy distribution of electrons scattered via the Compton process by gamma quanta with energies shown in the plot. The shown spectra include energy deposition resolution determined for the 30 cm long strips of the J-PET detector which is equal to $\sigma(E)/E = 0.044\sqrt{E(\text{MeV})}$ (Moskal et al 2014a).
In the following sections, first we estimate time resolution limits for infinitesimally small detector making an idealistic assumption that the time of arrival of each photon can be measured and used for the estimation of the time of gamma quantum interaction. We use Fisher information from all emitted photons and calculate the Cramér-Rao lower limit (DeGroot 1986, Seifert et al. 2012a) which is independent of the estimator used for the time resolution determination. Such estimations of the lower bound for the time resolution have been published recently (Seifert et al. 2012a) for small size crystals, taking into account the transit time spread of photomultipliers and neglecting the spread of the transit time inside scintillators. In this article we extend these investigations to the plastic scintillators strips with the length of up to 100 cm and include in the estimations the transit time spread due to the propagation of photons in scintillator strips as well as the transit time spread of photomultipliers. Further on we determine the lower bounds for the time resolution using a weighted mean of timestamps as an estimator of the time of the gamma quantum interaction. Next, we describe parameters used in the realistic simulations, including time distribution of photons emitted in ternary plastic scintillators, losses and time spread of photons due to their propagation through the scintillator, as well as quantum efficiency and transit time spread of photomultipliers. We test the simulation procedures by comparing simulated and experimental results for the BC-420 plastic scintillator read out at two ends by Hamamatsu R5320 photomultipliers. Section 7 contains description of the main idea of this article where the estimator of the time of the gamma quantum interaction is defined based on the time ordered set including timestamps from first photons registered by the matrix of SiPM converters. In this section we perform realistic simulations for the BC-420 scintillator strip and various configurations for the arrays of S12572-100P Hamamatsu silicon photomultipliers. Finally we estimate time resolution as a function of the scintillator length for the multi-SiPM readout allowing to determine timestamps of 20 photons. The results are compared to the resolutions achievable with the traditional readout with the vacuum tube photomultipliers.

The light yield of plastic scintillators amounts to about 10 000 photons per 1 MeV of deposited energy. Annihilation gamma quanta (0.511 MeV) used for the positron emission tomography interact with plastic scintillators predominantly via Compton scattering (Szymański et al. 2014), and therefore may deposit maximally an energy of 0.341 MeV (2/3 of electron mass). This corresponds to the emission of about 3410 photons. On the other hand, in order to decrease the noise due to the scattering of gamma quanta inside a patient body a minimum energy deposition of about 0.2 MeV is required (Moskal et al. 2012). Therefore, number of emitted photons discussed hereafter in this article includes the range from 2000 to 3410 photons.
2. Estimator of hit-time resolution (variance)

A single detection module considered in this article consists of the plastic scintillator strip connected at two ends to photomultipliers (see figure 3). We assume that the gamma quantum or any other particle of interest interacts in the scintillator at time $\Theta$. We consider the resolution for the reconstruction of the value of $\Theta$ based on time measurement of signals generated by photosensors attached to two scintillator ends. For practical reasons, if applicable, we use notation analogous to the one introduced in Seifert et al. (2012a).

In general, timestamps of all photons detected at the left ($t_{l1}, t_{l2}, ..., t_{lN}$) and at the right side ($t_{r1}, t_{r2}, ..., t_{RN}$) of the scintillator may be used for the estimation of the time of the interaction $\Theta$. It is advantageous to order the sets of timestamps according to ascending time such that:

\[ t_{li} < t_{lj} \leq \cdots \leq t_{li} \]

where indices in brackets indicate timestamps from the ordered set. The $t_{li}$ element in the ordered set is referred to as $i$-th order statistic (Seifert et al. 2012a). After ordering, the timestamps on one side become correlated but the ordered set allows for the simple and intuitive estimation of time difference between the signal arrivals to the ends of the scintillator:

\[ \Delta t_{li} = t_{li} - t_{ri} \]  

as well as interaction time $\Theta$ which may be estimated by:

\[ \Theta_{li} = \frac{t_{li} + t_{ri}}{2} + \text{const}_{li} \]

where \text{const}_{li} is subject to calibration and for simplicity, but without loss of generality, it will be omitted in the further considerations. Distributions of ordered timestamps at one side (e.g. $t_{li}$ and $t_{rj}$ for $i \neq j$) are correlated and not identical. However, distributions for the same order statistics at left and right side ($t_{li}$ and $t_{ri}$) are uncorrelated since the ordering at left side was done independently of the ordering at right side. Hence, it follows that variances of $\Delta t_{li}$ and $\Theta_{li}$ may be expressed as:

\[
\sigma^2(\Delta t_{li}) = \sigma^2(t_{li}) + \sigma^2(t_{ri}) - 2\text{cov}(t_{li}, t_{ri}) = \sigma^2(t_{li}) + \sigma^2(t_{ri}),
\]

\[
\sigma^2(\Theta_{li}) = \frac{1}{4}(\sigma^2(t_{li}) + \sigma^2(t_{ri}) + 2\text{cov}(t_{li}, t_{ri})) = \frac{1}{4}(\sigma^2(t_{li}) + \sigma^2(t_{ri})).
\]

The above equations imply that:

\[
\sigma^2(\Delta t_{li}) = 4\sigma^2(\Theta_{li}) = \sigma^2(t_{li}) + \sigma^2(t_{ri})
\]

We have checked this supposition by numerical simulations for the probability density distributions of emission times considered in this article. Therefore, as regards the variance, it is sufficient to study properties of only one of these estimators. Moreover, in order to facilitate direct comparison with results published in the field of TOF-PET we will express resolution as FWHM of coincidence resolving time (CRT), where coincidence resolving time determined for $i$-th order statistic will be referred to as CRT$_{li}$. It should be, however, noted that in general, even though $t_{li}$ and $t_{ri}$ are uncorrelated, the $\Delta t_{li}$ and $\Theta_{li}$ may be correlated since \text{cov}($\Delta t_{li}, \Theta_{li}$) = $(\sigma^2(t_{li}) - \sigma^2(t_{ri}))/2$ is equal to zero only if the emission point is in the center of the detector because only in this case the $t_{li}$ and $t_{ri}$ are identically distributed.

In next sections we define the emission time distribution for the plastic scintillators and estimate the Cramér–Rao lower limit for the achievable time resolution. Further on we will
simulate time resolution for each order statistics $\Delta t_{l(i)}$ separately, and we will test the variance of the weighted mean of $\Delta t_{l(i)}$ values showing that such estimator of $\Delta t$ allows to reach significantly better resolution than achievable with single order statistics.

3. Emission time distributions

In case of the ternary plastic scintillators, as e.g. BC-420 (Saint Gobain Crystals 2016) and its equivalent EJ-230 (Eljen Technology 2016) used in the J-PET detector, the distribution of the time of the photon emission followed by the interaction of the gamma quantum at time $\Theta$ can be well approximated by the following convolution of gaussian and exponential terms (Moszynski and Bengtson 1977, 1979):

$$f(t|\Theta) = K \int_{\Theta}^{\infty} \left( e^{- \frac{t-t_{r}}{\tau}} - e^{- \frac{t-t_{r}+t_{d}}{\sigma}} \right) \cdot e^{- \frac{(t-\Theta-2.5\sigma)^{2}}{2\sigma^{2}}} \, dt,$$

where the gaussian term with the standard deviation $\sigma$ reflects the rate of energy transfer to the primary solute, whereas $t_{r}$ and $t_{d}$ denote the average time of the energy transfer to the wavelength shifter, and decay time of the final light emission, respectively (Moszynski and Bengtson 1977, 1979). $K$ stands for the normalization constant ensuring that $\int_{\Theta}^{\infty} f(t|\Theta) \, dt = 1$. We have set $t_{d} = 1.5$ ns and treated $t_{r}$ and $\sigma$ as a phenomenological parameters and adjusted their values to: $t_{r} = 0.005$ ns, $\sigma = 0.2$ ns in order to describe the properties of the light pulses from the BC-420 scintillator i.e. rise time of 0.5 ns, decay time $t_{d} = 1.5$ ns and FWHM of 1.3 ns (Saint Gobain Crystals 2016). The resultant distribution of the emission time is indicated by the black solid line in figure 4. Other lines in this figure correspond to time distributions of
photons in the scintillator with the cross section of 0.5 cm × 1.9 cm simulated at various distances from the interaction point. These distributions will be used in the next section for the estimation of the lower limits of the achievable time resolutions.

4. Cramér–Rao lower limit on the resolution of hit-time reconstruction

The time resolution achievable with the scintillator detectors is limited by the optical and electronic time spread caused by the detector components, and by the time distribution of photons contributing to the formation of electric signals. The latter depends on the number of registered photons and is referred to as the photon counting statistics (Seifert et al 2012a). Limitations of the time resolution due to the photon counting statistics have been studied in detail e.g. in Seifert et al (2012a), (2012b), Spanoudaki and Levin (2011) and Fishburn and Charbon (2010) and the comprehensive account on this topic may be examined e.g. in Seifert et al (2012a). To large extent this research is driven by the endeavor to improve the timing properties of the PET systems (Kuhn et al 2006, Schaart et al 2009, Conti et al 2009, Schaart et al 2010, Moszynski and Szczesniak 2011, Lecoq et al 2013), and therefore so far the investigations concentrated on the small size crystal scintillators. In the recent work a detailed elaboration of the lower bound for time resolution has been published for most kinds of available crystal scintillators (Seifert et al 2012a). The estimation included transit time spread of photomultipliers but the spread due to the transport of photons inside the scintillators was neglected. This was justified since only small size crystals (in the order of 1 cm or smaller) were considered. Here, inspired by the new solution for the PET system based on plastic scintillators (Moskal et al 2011, 2014a, Raczyński et al 2014, Moskal et al 2015, Raczyński et al 2015), we extend the studies of Seifert and coauthors (Seifert et al 2012a) from the small size crystals to the large size plastic scintillators. In this section we estimate the lower limit of the time resolution achievable with scintillator strips of up to 100 cm assuming ideal electronic systems, and further on in the following sections we describe results of realistic simulations conducted taking into account both photon transport in scintillator material and transit time spread in photomultipliers.

The variance of any unbiased estimator Ξ of the hit-time Θ satisfies the Cramér–Rao inequality (DeGroot 1986, Seifert et al 2012a):

\[ \text{var}(\Xi) \geq \frac{1}{I_\Theta(\Theta)}, \] (7)

where \( I_\Theta(\Theta) \) denotes the Fisher information concerning \( \Theta \) in the set of \( N \) randomly chosen timestamps. This very general formula enables calculation of the lower bound of the variance of unbiased estimator. In case of point estimation of a parameter it quantitatively informs about the estimation efficiency and whether there is room for improvement. Knowing the probability density distribution of the photon registration time \( t \) following the gamma quantum interaction time \( \Theta \): \( f(t(\Theta)) \), the Fisher information in the sample of \( N \) independent timestamps reads (DeGroot 1986, Seifert et al 2012a):

\[ I_\Theta(\Theta) = N \int_{-\infty}^{+\infty} \left( \frac{\partial}{\partial \Theta} \frac{f(t(\Theta))^2}{f(t(\Theta))} \right) dt \] (8)

Figure 5 shows the lower limit of the time resolution estimated as a function of the number of registered photons \( N \) based on relations (7) and (8). Thick-solid line shows results assuming that the time distribution of registered photons is the same as the emission time distribution indicated by the thick solid line in figure 4. The other lower limits shown with thick-dashed,
thin-solid and thin-dashed lines were obtained assuming time distributions of photons after passing a distance of 30 cm, 50 cm and 100 cm of the plastic scintillator strip with a cross section of $0.5 \text{ cm} \times 1.9 \text{ cm}$. The corresponding time distributions are shown in figure 4.

In the limit of only one photon the result is quite intuitive since in this case the Cramér–Rao lower bound corresponds to about 3 ns which is approximately in the order of the FWHM of the time distribution of the emitted photons (solid line in figure 4) amounting to $\sim 3.5$ ns. The superimposed square indicates an experimental result obtained for the strip of BC-420 plastic scintillator with the dimensions of $0.5 \text{ cm} \times 1.9 \text{ cm} \times 30 \text{ cm}$ read out by Hamamatsu R5320 photomultipliers (Moskal et al 2014a). A comparison with the corresponding lower limit implies that there is still room for the substantial improvement of the time resolution. In the next sections we will present a novel solution which allows to improve the time resolution by more than a factor of 1.5.

5. Time resolution as a function of the order statistics for the ideal plastic scintillator

In this section we consider an ideal plastic scintillator detector where all emitted photons are registered by the two ideal photosensors (either left or right) with ideal time resolution and 100% quantum efficiency. It is also assumed that there is no photon absorption and no time spread in the infinitely small plastic scintillator. In figure 6 filled symbols show how the coincidence resolving time for first, second and third order statistic changes as a function of the number of emitted photons, and figure 7 illustrates how CRT varies as a function of order statistic in the case of 3000 emitted photons. As expected from the shape of the probability density distribution of emitted photons (figure 4) the average time difference between emitted photons decreases and hence the time resolution improves with the growing order statistic.
up to the time when the probability of emission of photons acquires maximum and then time resolution starts to worsen since the average time interval between emitted photons increases. Having timestamps from all registered photons, in the simplest way we can estimate the hit-time \( \Theta \) and time difference \( \Delta t \) e.g. as weighted means of corresponding values determined for all ordered statistics:

\[
\Theta \equiv \frac{\sum_i \frac{\Theta_i}{\sigma^2(\Theta_i)}}{\sum_i \frac{1}{\sigma^2(\Theta_i)}} = \frac{\sum_i \frac{i^{\Theta_i}}{2\sigma(\Theta_i)^2}}{\sum_i \frac{1}{\sigma(\Theta_i)^2}} + \frac{\sum_i \frac{\partial^2}{\sigma^2(\Theta_i)}}{\sum_i \frac{1}{\sigma^2(\Theta_i)}}
\]  

(9)
Coincidence resolving time $\text{CRT}_{(ij)}$ is presented in figure 6 as a function of number of emitted photons assuming the probability density distribution for plastic scintillator BC-420 (solid line in figure 4).

These calculations allow us to find out what is the best limit of time resolution for the considered detection systems when the hit-time is estimated as a weighted mean of the registered timestamps. Results shown in figure 6 imply that in principle for the energy deposition in the range from 0.2 MeV (2000 photons) to 0.341 MeV (3410 photons) a coincidence resolving time is equal to about $\text{CRT} = 0.042$ ns.

In the following section we will present results of simulations for the solution presently used in the J-PET detector and compare them with the experimental results. Further on simulations with a matrix SiPM readout will be presented and discussed.

6. Time resolution for the single module of the J-PET detector

The realistic simulations of the timestamps registered by the large size scintillator detectors require a proper account for the emission time distribution, photon transport and absorption inside the scintillator, as well as quantum efficiency and transit time spread of photosensors. All these effects have been taken into account as it is described in detail in the appendix A. In this section in order to test the simulation procedures we present results for the plastic scintillator BC-420 with dimensions of $0.5 \, \text{cm} \times 1.9 \, \text{cm} \times 30 \, \text{cm}$ read out at two ends by the Hamamatsu R4998 (R5320) photomultipliers. Recent measurements conducted with such detector revealed that about 280 photoelectrons are produced from the emission of about 3410 photons corresponding to the maximum energy deposition of the 0.511 MeV gamma quanta via the Compton effect (Moskal et al 2014a). This is very well reproduced in the simulations as can be inferred from figure 8 by a comparison of values at the upper and lower horizontal axes. Figure 8 shows dependence of the time resolution for the first, second and third order statistic as a function of the number of emitted photons. The result is consistent with the experimental value of CRT equal to about 0.266 ns obtained when determining time at the threshold $-50 \, \text{mV}$ of the leading edge of signals corresponding to the range of number of emitted photons between 2000 and 3410 (Moskal et al 2014a). Figure 8 indicates that in this range the experimental time resolution of 0.266 ns is between the values of time resolutions simulated for the first and third order statistics. This is as expected since predominantly only the first few photoelectrons contribute to the onset of the leading edge of photomultiplier signals. The obtained result shows that in practice the time resolution achievable from the leading edge may be estimated as a mean of resolutions for first and third order statistics. It is also interesting to note that for the discussed detector the best time resolution would be obtained by the measurement of the tenth ordered statistic (figure 9).

7. Time resolution for plastic scintillator read out by matrices of silicon photomultipliers

In the previous sections it was shown that the time resolution may be significantly improved by recording individual timestamps of photons arriving to the scintillator edge. In this section we present simulation of timing properties achievable for the long plastic scintillator...
strips equipped with readouts at two sides in the form of a matrix of silicon photomultipliers arranged as depicted in figure 3. The simulations have been performed assuming properties of the Hamamatsu S12572-100P silicon photomultiplier (Hamamatsu 2016) with photosensitive area of \(0.3 \times 0.3\) cm and the width of non-sensitive rim of 0.05 cm, and assuming that the scintillator has dimensions of \(0.7 \times 1.9 \times 30\) cm. A \(2 \times 5\) SPM matrix
as shown in figure 3) enables to cover with the photo-sensitive area about 68% of the end of scintillator with the cross section of $0.7 \text{ cm} \times 1.9 \text{ cm}$. Such matrices of photomultipliers enable to group photons reaching the end of the scintillator into ten subsamples on the left side: $(t_{1,1}^L, t_{2,1}^L, \ldots, t_{N_{111},1}^L)$, ..., $(t_{10,1}^L, t_{10,2}^L, \ldots, t_{10,N_{101},1}^L)$ and ten subsamples on the right side: $(t_{1,1}^R, t_{2,1}^R, \ldots, t_{N_{11R},1}^R)$, ..., $(t_{10,1}^R, t_{10,2}^R, \ldots, t_{10,N_{10R},1}^R)$, where first lower index denotes the ID of SiPM and the second lower index denotes the ID of the photon. Figure 10 shows that the photons are homogeneously distributed among different photomultipliers and (in the case of the maximum energy deposition by 0.511 MeV gamma quanta) on the average about 22 photons are registered by each SiPM.

Further on, we assume that a timestamp available from a given SiPM corresponds to the time of the fastest photon from the subsample registered by this photomultiplier. Therefore, for each subsample separately, we order timestamps according to ascending time such that: $(t_{1,1}^L, t_{2,1}^L, \ldots, t_{N_{111},1}^L)$, ..., $(t_{10,1}^L, t_{10,2}^L, \ldots, t_{10,N_{101},1}^L)$, and analogously for the right side, where indices in brackets indicate timestamps from the ordered subsample. The fastest times-tamps in subsamples: $(t_{1,1}^L, t_{2,1}^L, \ldots, t_{N_{111},1}^L)$ and $(t_{1,1}^R, t_{2,1}^R, \ldots, t_{N_{11R},1}^R)$ are considered as timestamps registered by the photomultipliers (hereafter referred to as photomultiplier’s timestamps). Next, for the left and right readout separately, we order the photomultiplier’s timestamps according to ascending time such that: $(t_{1,1}^L, t_{2,1}^L, \ldots, t_{N_{111},1}^L)$, ..., $(t_{10,1}^L, t_{10,2}^L, \ldots, t_{10,N_{101},1}^L)$, where indices in square brackets indicate SiPM timestamps after ordering, and the $t_{i,j}$ element in this set will be hereafter referred to as i-th order SiPM statistic. For each ordered SiPM statistic the interaction time $\Theta_i$ and the time difference between the signal arrivals to the ends of the scintillator $\Delta t_i$ are estimated as follows:

$$\Delta t_i = t_{i,j}^L - t_{i,j}^R$$

and
where \( \Theta_{ij} \) will be omitted in the further considerations without loss of generality. Finally, using information available from all SiPMs we estimate the hit-time \( \Theta \) and the time difference \( \Delta t \) as the weighted mean of above defined \( \Theta_{ij} \) and \( \Delta t_{ij} \) values, respectively.

Results of the performed simulations are shown in figure 11. The number of photoelectrons expected for the maximum energy deposition of 0.511 MeV gamma quanta \( (N = 3410) \) is equal to about 440 and is much higher than 280 obtained with the present J-PET prototype. This increase is due to the higher quantum efficiency of S12572-100P silicon photomultipliers with respect to the R4998 (R5320) vacuum tube photomultipliers (see figure A3 in the appendix A). Nevertheless, the time resolution for the first SiPM order statistics is worse with respect to the one obtainable with the R4998 (R5320) photomultipliers because of the larger transit time spread of SiPM with respect to R4998 (R5320). However, due to the access to ten SiPM timestamps (available with the \( 2 \times 5 \) SiPM matrix readout), a coincidence resolving time of CRT \( \approx 0.180 \) ns can be achieved when using a weighted mean of the measured SiPM timestamps. This is an average value for the range of interest (from 2000 to 3400 photons). In order to test a dependence of the achievable time resolution on the number of the SiPM in the readout, a systematic simulations were conducted changing the number of SiPM from 2 to 21. Figure 12 shows CRT obtained for various SiPM configurations. The result indicates that the improvement of resolution saturates with the growing number of photomultipliers, and that the \( 2 \times 5 \) configurations allowing to read 20 timestamps constitutes an optimal solution and further increase of number of SiPM does not improve the resolution significantly.

As a final result in figure 13 a time resolution achievable with vacuum photomultipliers R4998 (R5320) is compared to the resolution achievable with the \( 2 \times 5 \) SiPM matrix readout for the length of the scintillators from 2.5 cm up to 100 cm. Both results are confronted with
the resolution limit simulated for the ideal photosensors allowing for the measurement of each photon reaching the end of the strip. The result presented in the figure indicates that the readout consists of photomultipliers characterized by time spread and quantum efficiency the same as the SiPM Hamamatsu S12572-100P but with the dimensions allowing to fully cover the scintillator with the sensitive area with the following readout configurations: $1 \times 2$ (filled circles), $1 \times 3$ (filled triangles), $2 \times 5$ (filled squares), $2 \times 7$ (filled inverted triangles), and $3 \times 7$ (filled lozenges). Open squares indicate results for the $2 \times 5$ configuration taking into account non-sensitive area of the S12572-100P SiPM (the same as in figure 11). The result does not include the time spread due to the unknown depth-of-interaction.

**Figure 12.** Coincidence resolving time as a function of number of emitted photons $N$ simulated for the BC-420 plastic scintillator with dimensions of $0.7 \text{ cm} \times 1.9 \text{ cm} \times 30 \text{ cm}$. In the simulations it was assumed that the readout consists of photomultipliers characterized by time spread and quantum efficiency the same as the SiPM Hamamatsu S12572-100P but with the dimensions allowing to fully cover the scintillator with the sensitive area with the following readout configurations: $1 \times 2$ (filled circles), $1 \times 3$ (filled triangles), $2 \times 5$ (filled squares), $2 \times 7$ (filled inverted triangles), and $3 \times 7$ (filled lozenges). Open squares indicate results for the $2 \times 5$ configuration taking into account non-sensitive area of the S12572-100P SiPM (the same as in figure 11). The result does not include the time spread due to the unknown depth-of-interaction.

8. Summary

The realistic simulations based on the Monte-Carlo method were conducted in order to estimate the time resolution achievable with the J-PET tomography scanner built from strips of plastic scintillators (Moskal et al 2011, 2014a, Raczy et al 2014, Moskal et al 2015, Raczyński et al 2015). The simulations took into account: (i) emission spectrum of the plastic scintillator BC-420 (EJ-230), (ii) probability density distribution of photon emission times, (iii) transport of photons along the scintillator strip, (iv) absorption of photons in the scintillator material, (v) spectrum of quantum efficiency of photosensors, and (vi) photomultipliers transit time spread. Arrangement of SiPM photosensors in the form of $2 \times 5$ matrix attached at two ends to the scintillator strip allowed for registering 10 timestamps at each side. These after ordering
according to the ascending time were used to estimate the time of interaction as a weighted mean of times registered for each ordered SiPM statistics. Exploitation of information on 10 timestamps at each side improved the time resolution with respect to the present readout based on vacuum tube photomultipliers by about a factor of 1.5 despite the fact that the transit time spread of the considered silicon photosensors S12572-100P ($\sigma_{TTS} = 0.128$ ns) is almost two times larger than TTS of photomultipliers R4998 (R5320) ($\sigma_{TTS} = 0.068$ ns) used in the present version of the J-PET detector.

For the energy loss in the range from 0.2 MeV to 0.341 MeV (corresponding to the emission of 2000 – 3410 photons), relevant for the positron emission tomography with plastic scintillators, it was shown that with the S12572-100P photosensors arranged into a $2 \times 5$ matrix at two ends of the scintillator strip the coincidence resolving time changes from CRT $\approx 0.170$ ns to CRT $\approx 0.365$ ns when extending an axial field-of-view from 15 cm to 100 cm. This corresponds to the changes of the axial position resolution from 1.4 cm (FWHM) to 3.1 cm (FWHM), respectively. However, as it is shown by solid circles in figure 13 there is still room for improving CRT and hence also for improving an axial position resolution by about a factor of two by decreasing the time-jitter of the SiPMs. The results open perspectives for construction of the cost-effective TOF-PET scanner with significantly better TOF resolution and larger field-of-view with respect to the newest TOF-PET modalities characterized by CRT $\approx 0.4$ ns (Philips 2016, General Electric 2016). In addition, a J-PET scanner built from long strips of plastic scintillators read out by the silicon photosensors, may be combined with the Magnetic Resonance Imaging modality in a way allowing for the simultaneous PET and MRI measurement with the large field-of-view (Moskal 2014b) e.g. by inserting a barrel built of plastic strips into the MRI system.

Figure 13. Coincidence resolving time as a function of the scintillator’s length for 2700 emitted photons in the center of the scintillator with the cross section of 0.7 cm × 1.9 cm. (Triangles) A mean value of CRT$_{11}$ and CRT$_{13}$ simulated for the scintillator read out at two ends by the Hamamatsu R4998 (R5320) photomultipliers. (Squares) CRT simulated for the scintillator read out at two ends by the matrix of $2 \times 5$ S12572-100P photomultipliers. (Circles) CRT determined as a weighted mean from all measured timestamps assuming ideal photosensors with no transit time spread and 100% quantum efficiency and assuming that there is no photon absorption in the scintillator material. The shown values take into account an additional smearing of the time due to the unknown depth of interaction. This can be well approximated by the FWHM equal to about 0.063 ns in the case of the 1.9 cm thick scintillators. The lines are shown to guide the eye.
Finally, it was shown that not only an intrinsic lower bound for the time resolution calculated using the Fisher information and Cramér-Rao inequality, but also more practical limit determined for the time estimated as a mean of all timestamps registered with the ideal photosensor is much lower than the above quoted resolutions. Therefore, there is still room for further improvement of the TOF resolution of the J-PET tomograph which can be achieved anticipating future availability of silicon photosensors with transit-time-spread lower than $\sigma(TTS) = 0.128$ ns of S12572-100P Hamamatsu photomultipliers.

The main purpose of the development of the J-PET system is to find a cost-effective way of the whole body PET imaging. Thus, in order to compare the performance of the J-PET with the presently available LSO based TOF-PET devices, by analogy to Conti (2009) and Eriksson and Conti (2015) we introduce a following formula expressing a figure-of-merit $FOM_{wb}$ relevant for the whole body imaging:

$$FOM_{wb} = \epsilon_{\text{detection}}^2 \times \epsilon_{\text{selection}}^2 \times Acc / (CRT \times N_{\text{steps}}),$$

where $\epsilon_{\text{detection}}$ denotes the detection efficiency of a single 0.511 MeV gamma quantum, $\epsilon_{\text{selection}}$ indicates the selection efficiency of ‘image-forming’ events, CRT denotes the coincidence resolving time, $N_{\text{steps}}$ indicates number of steps (bed positions) needed to scan a whole body, and $Acc$ denotes a geometrical acceptance.

In the first order of approximation we may assume that $N_{\text{steps}}$ is inversely proportional to the AFOV, and that the term $\epsilon_{\text{detection}}^2 \times Acc$ is proportional to the $\int_{\theta_{\text{min}}}^{\theta_{\text{max}}} (\epsilon_{\text{detection}}/\sin \theta)^2 \sin \theta d\theta$, where $\theta$ denotes the angle between the direction of the gamma quanta and the main axis of the tomograph; the term $\epsilon_{\text{detection}}/\sin \theta$ accounts for the changes of the detection efficiency as a function of the $\theta$ angle, with $\epsilon_{\text{detection}}$ denoting detection efficiency when gamma quantum crosses the detector perpendicularly to its surface; $\sin \theta d\theta$ stands for the angular dependence of the differential element of the solid angle, and $\theta_{\text{min}}$ to $\theta_{\text{max}}$ determines the range of angular acceptance of the tomograph. The above assumptions yield:

$$FOM_{wb} = \int_{\theta_{\text{min}}}^{\theta_{\text{max}}} (\epsilon_{\text{detection}}/\sin \theta)^2 \sin \theta d\theta \times \text{AFOV} / \text{CRT}. \quad (14)$$

Figure 14 shows the ratio $R$ of $FOM_{wb}$ of the J-PET and LSO based PET detectors defined as: $R(\text{AFOV-J-PET}) = FOM_{wb}(\text{AFOV-J-PET})/FOM_{wb}(\text{LSO with AFOV} = 20 \text{ cm})$. The shown ratio is determined for a fixed AFOV = 20 cm of the LSO based PET, but varying the AFOV of the J-PET detector. Full dots indicate result determined for a single J-PET layer ($N_{\text{layers}} = 1$), and open squares indicate result for J-PET with two layers ($N_{\text{layers}} = 2$). The results shown in figure 14 were obtained assuming a 2 cm radial thickness of the detection layers and taking into account that linear attenuation coefficients of 0.511 MeV gamma quanta are equal to $\mu_{\text{LSO}} = 0.87 \ \text{cm}^{-1}$ (Mechler 2000) and $\mu_{\text{plastic}} = 0.098 \ \text{cm}^{-1}$ (Saint Gobain Crystals 2016). Furthermore it was assumed that (i) CRT of LSO based scanners is equal to 0.4 ns as achieved recently by manufacturers Philips (Philips 2016) and General Electric (General Electric 2016), and that (ii) $\epsilon_{\text{selection}}$ for LSO is equal to 0.32, which is a fraction of the photoelectric effect in the case of the LSO crystals (Humm et al 2003), and that (iii) $\epsilon_{\text{selection}}$ of the J-PET is equal to 0.44 which corresponds to the fraction of events with energy deposition larger than 0.2 MeV in the case of plastic scintillators. Figure 14 indicates that in order to compensate for the lower efficiency of plastic scintillators and thus to obtain $FOM_{wb}$ of the J-PET comparable to the LSO based scanners with AFOV = 20 cm it is required to use either two detection layers or to increase the J-PET AFOV to about 50 cm. Certainly the $FOM_{wb}$ of the LSO based PET would also grow approximately as square of AFOV but at the same time
the cost of such PET detector would increase almost linearly proportional to AFOV, whereas the cost of the J-PET does not increase significantly when increasing the AFOV.

The relative ease of the cost effective increase of the axial field-of-view makes the J-PET tomograph competitive with respect to the current commercial PET scanners as regards sensitivity and time resolution, yet this is achieved at the expense of the significant reduction of the axial spatial resolution. Finally, it is worth to stress that the J-PET with a long diagnostic chamber opens unique perspectives for simultaneous whole-body metabolic imaging not accessible with the presently available PET/CT modalities.

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Appendix A. Simulation of photon transport in cuboidal scintillator strips

In a long scintillator strip, a photon on its way from the emission point to the photomultiplier may undergo many internal reflections whose number strongly depends on the scintillator size and the photon emission angle. However, the space reflection symmetries of the cuboidal shapes, which are considered in this article, enables a significant simplification of the photon transport algorithm, without following photon propagation in a typical manner. In our simulations for each emitted photon the initial direction of its flight is obtained in polar coordinate system as two uniformly distributed random values of $\cos \theta$ and $\sin \theta$, where $\theta$ is the angle between flight direction and $z$-axis and $\phi$ is the azimuthal angle as defined in standard spherical coordinate system. The coordinate system is defined in figure 3 where the $z$-axis is directed along the longest axis of the scintillator strip. The components of photon flight direction vector can be expressed as follows:

$$ \text{dir} = [\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta] $$

(A.1)

The number of reflections from the side surfaces that are normal to $x$ or $y$-axis are calculated using the projection of the flight-direction vector to $y$-$z$ or $x$-$z$-plane, respectively:

$$ \tan \theta_x = \frac{\text{dir}_y}{\text{dir}_z}; \tan \theta_y = \frac{\text{dir}_x}{\text{dir}_z}, $$

(A.2)

where $\theta_x$ is the angle between $\text{dir}$ projection on $x$-$z$-plane and $z$-axis and $\theta_y$ is the same for projection on $y$-$z$-plane.

Taking into account the fact that each reflection changes only the sign of respective component of $\text{dir}$ we can assume that the reflection angle is not changed for each pair of side surfaces during the whole photon flight. So we need to obtain two values of reflection angle: one for side surfaces normal to $x$-axis and one for ones normal to $y$-axis. Knowing that $|\text{dir}| = 1$ and that these are the angles between photon flight direction and the normal vectors for respective side surfaces ($x$ and $y$ axes) we obtain:

$$ \cos \alpha_x = \text{dir}_x; \cos \alpha_y = \text{dir}_y, $$

(A.3)

where $\alpha_x$ and $\alpha_y$ are the reflection angles for side surfaces normal to respective axis. Then the probability of photon’s reaching the photomultiplier can be calculated using a following formula:

$$ P_{\text{reach}} = P_{\text{refl}}(\sin \alpha_x)^{n_x}P_{\text{refl}}(\sin \alpha_y)^{n_y}, $$

(A.4)

where $n_x$ and $n_y$ denote the respective numbers of reflections. The dependence $P_{\text{refl}}(\sin \alpha)$ is obtained from Fresnel equations and is shown in figure A1.

Further factors that influence the photon registration probability are absorption in the scintillator material, losses at surface imperfections, and the photomultiplier’s quantum efficiency. In current algorithm of simulation the following formula for photon registration probability has been used

$$ P_{\text{reg}} = P_{\text{reach}} \epsilon(\lambda) e^{\frac{-\mu_{\text{eff}}(\lambda) L}{\cos \theta}} $$

(A.5)

where $P_{\text{reach}}$ denotes the probability from formula (A.4), $\lambda$ denotes the photon’s wavelength, $\epsilon(\lambda)$ stands for the photomultiplier’s quantum efficiency and $\mu_{\text{eff}}(\lambda)$ is the effective absorption coefficient for the scintillator material. The latter, shown by thick solid line in figure A2, accounts effectively for the absorption of photons on the way to photomultipliers and was determined by scaling the absorption coefficient of pure polystyrene (Senchyshyn et al 2006)
to the experimental results obtained with the single detection unit of the J-PET detector (Kowalski et al 2015). The scaling factor accounts effectively for the absorption due to the primary and secondary admixture in the scintillator material, imperfections of surfaces and reflectivity of the foil (Kowalski et al 2015). It was determined by the comparison of simulations with experimental results obtained for the EJ-230 plastic scintillator with dimensions of 0.5 cm × 1.9 cm × 30 cm (Kowalski et al 2015).

Photomultipliers quantum efficiencies that were used in current calculations are shown in figure A3.

The time of arrival $t_{\text{arrival}}$ of $i$th photon at the photomultiplier (or in general the time of passing a given distance $\Delta L$ along the scintillator) may be expressed as:
\[ t'_{\text{arrival}} = t'_i + \frac{\Delta L}{\pi \cos \theta}, \]  

(A.6)

where \( t'_i \) is the emission time of \( i \)th photon, \( \Delta L \) denotes the distance between the emission point and the photomultiplier, \( c \) denotes the speed of light and \( n \) stands for scintillator’s refractive index (the value of \( n = 1.58 \) was used) (Saint Gobain Crystals 2016).

Finally, the timestamp \( t_i \) is simulated by smearing the time \( t'_{\text{arrival}} \) taking into account the transition time spread of the photosensors:

\[ t_i = t'_{\text{arrival}} + RG(t_{\text{offset}}, \sigma), \]  

(A.7)

where \( RG(0, \sigma) \) is value generated randomly according to the Gauss distribution with the mean at \( t_{\text{offset}} \), and with standard deviation \( \sigma \) equal to the standard deviation of time spread of a given photomultiplier. For simulations referred to in this paper as done with ‘ideal photomultiplier’ \( \sigma = 0 \). Otherwise for Hamamatsu R4998 (R5320) photomultiplier \( \sigma = 0.068 \) ns (Hamamatsu 2016) and for silicon photomultiplier S12572-100P \( \sigma = 0.128 \) ns (Hamamatsu 2016). The parameter \( t_{\text{offset}} \) accounts for all constant electronic time delays and its value does not influence the time resolution. Therefore, for simplicity, but without loss of generality, it is set to zero.

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Figure A3. Quantum efficiency as a function of photon’s wavelength for Hamamatsu R4998 (R5320) photomultiplier (Baszak 2014) (solid line) and Hamamatsu silicon S12572-100P photomultiplier (dashed line). A superimposed thin solid line denotes emission spectrum of the Saint Gobain BC-420 plastic scintillator. The left axis denotes quantum efficiency and right axis denotes the emission intensity.
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