Analysing and Modelling the Performance of the 
HemeLB Lattice-Boltzmann Simulation Environment

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Abstract

We investigate the performance of the HemeLB lattice-Boltzmann simulator for cerebrovascular blood flow, aimed at providing timely and clinically relevant assistance to neurosurgeons. HemeLB is optimised for sparse geometries, supports interactive use, and scales well to 32,768 cores for problems with ~81 million lattice sites. We obtain a maximum performance of 29.5 billion site updates per second, with only an 11% slowdown for highly sparse problems (5% fluid fraction). We present steering and visualisation performance measurements and provide a model which allows users to predict the performance, thereby determining how to run simulations with maximum accuracy within time constraints.

Keywords: lattice-Boltzmann, parallel computing, high-performance computing, performance modelling

1. Introduction

Recent progress in imaging and computing technologies has resulted in an increased adoption of computational methods in the life sciences. Using modern imaging methods, we are now able to scan the geometry of individual vessels within patients and map out potential sites for vascular malformations such as intracranial aneurysms. Likewise, recent increases in computational capacity and algorithmic improvements in simulation environments allow us to simulate blood flow in great detail. The HemeLB lattice-Boltzmann application aims to combine these two developments, thereby allowing medical
scans to be used as input for blood flow simulations. It also enables clinicians to run such simulations in real-time, providing runtime visualisation feedback as well as the ability to steer the simulation and its visualisation [2]. One principal long-term goal for HemeLB is to act as a production toolkit that provides both timely and clinically relevant assistance to surgeons. To achieve this we must not only perform extensive validation and testing for accuracy, reliability, usability and performance, but also ensure that the legal environment and the medical and computational infrastructure are made ready for such use cases [3].

In this work we investigate the performance aspects of the HemeLB environment, taking into account the core lattice-Boltzmann (LB) simulation code and the visualisation and steering facilities. We present performance measurements from a large number of runs using both sparse and non-sparse geometries and the overheads introduced by visualisation and steering. Medical doctors treating patients with intracranial aneurysms are frequently confronted with very short time scales for decision-making. For HemeLB to be useful in such environments, it is therefore not only essential that the code simulates close to real-time, but also that the length of a simulation can be reliably predicted in advance. We demonstrate that it is possible to accurately characterise CPU and network performance at low core counts and integrate this information into a model that predicts performance for arbitrary problem sizes and core counts.

1.1. Overview of HemeLB

HemeLB is a massively parallel lattice-Boltzmann simulation framework that allows interactive use, eventually in a medical environment. Segmented angiographic data from patients can be read in by the HemeLB Setup Tool, which allows the user to indicate the geometric domain to be simulated using a graphical user interface. The geometry is then discretised into a regular grid, which is used to run HemeLB simulations. The core HemeLB code, written in C++, consists of a parallelised lattice-Boltzmann application which is optimised for sparse geometries such as vascular networks by use of indirect addressing. We precompute the addresses of neighbouring points within a single one-dimensional array instead of requiring that the points be stored in a dense, three-dimensional array. HemeLB also constructs a load-balanced domain decomposition at runtime, allowing the user to run simulations at varying core counts with the same simulation domain data. HemeLB is highly scalable due to a well-optimised communication strategy and the locality of
interactions and communications in the parallelised lattice-Boltzmann algorithm. The File I/O operations are done in parallel using MPI-IO by a group of reading processes, which can be adjusted in size using a compile-time parameter.

The HemeLB Steering Client is a light-weight tool that allows users to connect remotely to their HemeLB simulation, receive real-time visual feedback and modify parameters of the simulation at runtime. Here, the visualisations are generated on-site within HemeLB, using a hand-written ray-tracing kernel [2]. In our work we run HemeLB with the steering server code enabled. As a result, one core is reserved for steering purposes, whether or not a client is connected, and is thereby excluded from the LB calculations.

HemeLB relies on ParMETIS version 4.0.2 [4] to perform its domain decomposition. It constructs an initial guess using a basic graph growing partitioning algorithm (see Mazzeo et al. [1] for details), which it then passes to ParMETIS for optimisation using the ParMETIS_V3_PartKway() function. Constructing the initial guess requires less than a second of runtime in all cases, but the ParMETIS optimisation typically adds between 5 and 30 seconds to the initialisation time. We discuss several technical aspects and performance implications of our decomposition routine in Section 3.1.

HemeLB uses a coalesced asynchronous communication strategy to optimize its scalability [5]. This system bundles all communications for each iteration (e.g., exchanges required for the LB algorithm, steering and visualisations) into a single batch of non-blocking communication messages, one for each data exchange of non-zero size between a pair of processes in each direction. As a result, each iteration of HemeLB’s core loop has only one MPI_Wait synchronisation point, minimising the latency overhead of HemeLB simulations. Communication of variable length data is spread over two iterations, the sizes being transferred during the first iteration while the actual exchange takes place during the second one.

The coalesced communication system is also used for the phased broadcast and reduce operations which are required for the visualisation and steering functionality. Here HemeLB arranges the processes into an $n$-tree and, for broadcasts, sends data from one level of the tree to the level below over successive iterations. For reductions, data is sent up one level of the tree over successive iterations. Hence, both operations can take $O(\log(p))$ iterations, for $p$ cores. In this approach HemeLB does require some additional memory for communication buffers. Additionally, the responsiveness of the steering is constrained, as data arriving in the top-most node takes $O(\log(p))$ iterations.
1.2. Related work

A large number of researchers have investigated the performance aspects of various LB simulation codes over the past decade. These investigations have been done without real-time visualisation or steering enabled, and frequently use non-sparse geometries. We present a performance analysis of both sparse geometries and interactive usage modes in this work. Pohl et al. [6] compared the performance of LB codes across three supercomputer architectures, and concluded that the network and memory performance (bandwidth and latency) are dominant components in establishing a high LB calculation performance. Geller et al. [7] compared the performance of an LB code with that of several finite element and finite volume solvers, and deduced that LB offers superior efficiency in flow problems with small Mach numbers. Williams et al. [8] presented a hierarchical autotuning model for parallel lattice-Boltzmann, and report a performance increase of more than a factor 3 in their simulations. Several groups have considered the performance of LB solvers on general-purpose graphics processing unit (GPGPU) architectures. In these studies, they introduced a number of improvements, such as non-uniform grids [9], more efficient memory management strategies [10, 11] and LB codes which run across multiple GPUs [12, 13, 14]. Other performance investigations include a comparison between different LB implementations [15], hybrid parallelisations for multi-core architectures in general [16, 19, 17] and performance analysis of LB codes on Cell processors [18, 19, 20].

A few studies within the physiological domain are of special relevance to this work. These include a performance analysis of a blood-flow LB solver using a range of sparse and non-sparse geometries [21] and a performance prediction model for lattice-Boltzmann solvers [22, 23]. This performance prediction model can be applied largely to our HemeLB application, although HemeLB uses a different decomposition technique and performs real-time rendering and visualisation tasks during the LB simulations. Mazzeo and Coveney [11] studied the scalability of an earlier version of HemeLB. However, the current performance characteristics of HemeLB are substantially enhanced due to numerous subsequent advances in the code, amongst others: an improved hierarchical, compressed file format; the use of ParMETIS to ensure good load-balance; the coalesced communication patterns to reduce the overhead of rendering; use of compile-time polymorphism to avoid
virtual function calls in inner loops.

2. Performance analysis

We benchmarked HemeLB using simulation domains based on three distinct geometries, a vascular network (see Fig. 2 used to generate three simulation domains), a bifurcation of vessels (see Fig. 1 used to generate two simulation domains) and a cylinder. Both the network and the bifurcation geometries are sections of an intracranial vasculature model that has been constructed from multiple rotational angiography scans of a patient with an intracranial aneurysm treated at the U.K. National Hospital for Neurology and Neurosurgery. The third and least sparse geometry is an artificially created cylinder. We present an overview of the simulation domains we generated and use in our runs in Table 1. We also provide a brief description of the sparseness of each generated simulation domain. Our runs were impulsively started, applying a pressure gradient across the simulation domain, using Nash in-outlet conditions (Nash et al., in preparation).
Figure 2: Graphical overview of the network geometry in the HemeLB Setup Tool. We used this geometry to generate the Network, Large Network and Small Network simulation domains.

Table 1: Overview of the simulation domains used in our experiments. The percentage of the simulated box that consists of active fluid sites is given by the fluid fraction. Non-active fluid sites do not count towards the number of lattice sites in the simulation.

| Name             | # of lattice sites | fluid fraction |
|------------------|--------------------|----------------|
| Bifurcation      | 19,808,107         | 11%            |
| Cylinder         | 15,607,040         | 65%            |
| Network          | 18,836,545         | 5.1%           |
| Large Bifurcation| 81,132,544         | 11%            |
| Large Network    | 44,650,496         | 5.1%           |
| Small Network    | 77,182             | 5.1%           |

2.1. Performance of LB computations

We have run blood flow simulations using the simulation domains listed in Table 1 using up to 32,768 cores on the HECToR Phase 3 supercomputer at EPCC in Edinburgh, United Kingdom. The HECToR machine is a Cray XE6 with 90,112 cores (2.3GHz AMD Opteron 6276), and has a peak performance of 9.2 GFLOP/s per core. Our simulations were done using a 15-directional lattice-Boltzmann kernel (D3Q15), the Lattice Bhatnagar-
Gross-Krook [24] model with simple bounce-back boundary conditions and a fixed physical viscosity of 0.004 Pa s. We present the scalability results for all simulation domains in Figure 3. We find that the small network simulation domain scales near-linearly up to 128 cores, despite consisting of only 77,182 lattice sites. All of the medium-sized simulation domains (Bifurcation, Cylinder and Network) scale linearly to 8,192 cores. However, the communication overhead and load imbalance reduce the performance on higher core counts. The two largest simulation domains (Large Bifurcation and Large Network) show linear scaling from 512 cores up to 16,384 cores, and significant speedup to 32,768 cores, achieving a maximum performance of 29.5 billion site updates per second (SUPS). The performance obtained at 8,196 cores for the medium-sized bifurcation corresponds to 419 timesteps per second, or 646 times slower than real-time for a maximum timestep as limited by incompressibility constraints. The maximum timestep here is estimated by the need to keep the Mach number below 0.05, using a typical blood velocity for vessels of this size of 25 cm/s. At this rate, it takes HemeLB 553 seconds to simulate one heartbeat with a resolution of around 100 lattice points across a vessel diameter. We present the performance in SUPS per core as a function of the number of sites per core in Figure 4, demonstrating that the SUPS per core is largely independent of other factors.

2.2. Visualisation performance

One of the features that sets HemeLB apart from many other LB codes is its ability to perform in situ rendering of the geometry at runtime [2], using a parallelised ray-tracing algorithm. The communication needs of the ray-tracing algorithm have been combined with those of the main simulation algorithm, through the coalesced communication strategy, massively improving the scaling when rendering frames. The images rendered by HemeLB can either be stored on disk for future reference or they can be forwarded as a streaming visualisation to the steering client. In this section we present several simulations where we assess the overhead introduced by rendering images, as well as that introduced by writing snapshots of the simulation data. These snapshots store the hydrodynamic variables at each lattice point, recording all information of physical relevance which is useful for visualisation and post-processing. File I/O operations are done in HemeLB using a subset of all processes, the reading group. Within this work, we adopted a reading group size of 32 processes, or the number of processes used by HemeLB, whichever was smaller. We have run four types of simulations using the Bifur-
cylinder
network
bifurcation
large network
large bifurcation
small network
linear scaling

Figure 3: Lattice site updates per second (SUPS) as a function of the number of cores used for simulations run on the HECToR Cray XE6 machine. We run simulations using each of the six simulation domains (Cylinder, Network, Bifurcation, Large Bifurcation, Large Network and Small Network).

cation simulation domain, one with snapshots and image-rendering disabled, one where we write snapshots to disk (10 snapshots per 1000 time steps, with each snapshot being 604MB in size), one where we render and write images to disk (10 rendered images per 1000 time steps, with each image being 180kB in size) and one with both snapshots and images enabled. We have carried out the tests using 256, 512, 1024 and 2048 cores. We present our results in Fig. 3. Here the overhead for rendering and writing images is marginal, and adds no more than a few percent to the execution time in most cases. Simulations which have snapshot writing enabled are both considerably slower and have more variable performance, due to the high disk activity involved with snapshot writing. When snapshot writing is enabled, the overhead caused by image rendering is difficult to observe, as the standard deviation bars of the performance measurements with and without images overlap. When the simulation writes 10 snapshots over 1000 LB steps, we observe an increase in the wall-clock time of $\sim$24 seconds.
Figure 4: Site updates per second (SUPS) per core averaged over all cores used in the simulation (excluding the one used for steering) as a function of the number of sites per core, for six LB problems.

We have also run several simulations of 1000 LB steps where we render and write an image to disk every 5 to 200 LB steps. The results for these runs (which were done using 1024 and 2048 cores) are given in Fig. 6. Without rendering the simulations took 31.4, 16.1 and 7.81 seconds on 512, 1024 and 2048 cores respectively. We observe an overhead of less than two seconds per 1000 LB steps if we render and write no more than 10 images during that period. However, the performance deteriorates somewhat when we write more images, with a maximum measured overhead of \( \sim 6.5 \) seconds. We also again observe some jitter in our results, for example in the 1024 core simulation that rendered one image every 50 steps, which we attribute to fluctuations in the file system performance of the machine. Rendering one image per 5 LB steps using 2048 cores corresponds to a frame rate of about 13.6 frames per second, more than sufficient for smooth visualisations of the simulations in real time.
Figure 5: Time spent to simulate 100 time steps as a function of the number of cores used for four settings: no snapshots and no images (blue), images only (green), snapshots only (black) and snapshots and images (red). We averaged the results from runs including any form of snapshot or image writing over three executions, and included a standard deviation error bar with each data point.

2.3. Steering performance

The previous subsection isolates the performance impact of the visualisation and rendering, with images written to disk. Here we study the performance impact of the HemeLB steering component, using the Cylinder simulation domain, where images are streamed over the network to a client. In this case, HemeLB produces images as described in Section 2.2, optionally limited by a maximum frame-rate per second. We also look at the performance impact of sending steering messages from the client to the HemeLB steering component. In order to obtain reproducible data, the steering client is set up with a scripted set of simulated user actions (orbiting the viewpoint for image rendering). These results are presented in Table 2 and in Figure 7 and were produced with the steering client running on the HECToR login node. For a frame-rate of 4.6 frames per second, which is usable for scientific steering, with bidirectional communication between client and server,
corresponding to 32 LB steps per rendered image, we observe an overhead of 28%.

2.4. Performance comparison with other codes

In this section we compare the performance of HemeLB with performance measurements of other LB codes as found in the literature. We gathered the number of million lattice site updates per second (MSUPS), the standard measure of LB performance, reported for other implementations. HemeLB is strongly optimised for efficiently handling sparse geometries while most codes are not, making like-for-like comparison difficult. The other applications may not be capable of simulating even moderate complexity domains, such as a cylinder, at all or only at the cost of allocating memory to non-fluid sites. Additionally, the directional resolution affects the number of calcula-
Table 2: Performance impact of running HemeLB with a connected steering client, simulating the Cylinder simulation domain using 1024 and 2048 cores. Here the mode is the method of running HemeLB, which can be without client (none), with the client used only for image streaming (images) or with the client used both for image streaming and steering the HemeLB simulation (both).

| p  | mode  | frame-rate (1/s) requested | frame-rate (1/s) achieved | MSUPS per core | mean LB steps per image |
|----|-------|----------------------------|--------------------------|----------------|------------------------|
| 1024 | none   | -                          | -                        | -              | -                      |
| 1024 | both   | 2.0                        | 2.0                      | 1.28           | 41.5                   |
| 1024 | images | 2.0                        | 2.1                      | 1.25           | 39.3                   |
| 1024 | both   | 5.0                        | 4.4                      | 1.11           | 16.5                   |
| 1024 | images | 5.0                        | 4.8                      | 1.02           | 13.8                   |
| 1024 | both   | max                        | 5.9                      | 0.84           | 11.3                   |
| 1024 | images | max                        | 8.2                      | 0.76           | 6.0                    |
| 2048 | none   | -                          | -                        | -              | -                      |
| 2048 | images | 2.0                        | 2.1                      | 1.26           | 77.2                   |
| 2048 | both   | 2.0                        | 2.2                      | 1.32           | 78.6                   |
| 2048 | both   | 5.0                        | 4.6                      | 1.15           | 32.2                   |
| 2048 | images | 5.0                        | 4.8                      | 0.99           | 26.9                   |
| 2048 | images | max                        | 9.5                      | 0.59           | 8.0                    |
| 2048 | both   | max                        | 10.6                     | 0.66           | 8.1                    |

tions and memory accesses required per site update, as well as the presence of other special features, such as the additional presence of a D3Q15 magnetic field distribution model in LBMHD [8]. One particular example is LB3D [25], version 7, which calculates a number of additional forces, and is strongly optimised for multi-phase flow at the expense of single-phase flow performance. For LB3D we therefore included measurements for both single-phase and multi-phase flow performance.

We provide the LB performance configurations and results for several well-known LB codes in Tables 3 and 4. The MSUPS per core results here are obtained by dividing the total number of lattice site updates by the product of time spent on LB iterations and the number of cores. From each literature source, we picked the result from the run that showed the best MSUPS per core while running on at least one full processor. In the case of HemeLB we picked the best result from the non-sparse Cylinder, as well as from the very sparse Network and Large Network simulation domains, which
are the only measurements in the tables using sparse geometries.

When we examine bulk flow only, the MSUPS per core performance of HemeLB is comparable with that achieved with LBMHD (although LBMHD calculates in 27 directions and HemeLB in 15), and about half of that achieved with Palabos on similar AMD Opteron architectures. The performance of HemeLB, however, is almost entirely preserved when using a very sparse simulation domain as HemeLB does not allocate memory or computational effort for non-active lattice sites, which are by definition common in sparse geometries. LBMHD has no known optimisations for sparse geometries while Palabos features a partial optimisation using the multi-block method [26], of which we found no performance data using sparse geometries in the literature. The multi-block method is relatively inefficient because it allocates memory to some of the non-fluid sites and uses data structures that grow in complexity when off-lattice geometries are modelled more accurately.
Table 3: Technical specifications of 12 LB simulations in our code comparison. We provide the name of the LB application used in the first column (including the source), followed by respectively the architecture used for the simulations and the number of cores used for the run.

| Name                        | Architecture          | cores |
|-----------------------------|-----------------------|-------|
| HemeLB (Cylinder)           | AMD Opteron 6276 (9.2)| 4096  |
| HemeLB (Network)            | AMD Opteron 6276 (9.2)| 32    |
| HemeLB (Large Network)      | AMD Opteron 6276 (9.2)| 512   |
| LB3Dv7 (Shamardin p.c.)     | AMD Opteron 6276 (9.2)| 32    |
| LB3Dv7-3phase (Shamardin p.c.) | AMD Opteron 6276 (9.2)| 128   |
| LBMHD [8]                   | AMD Opteron 1356 (9.2)| 8192  |
| LBMHD [8]                   | AMD Opteron 6172 (8.4)| 49152 |
| LUDWIG [14]                 | AMD Opteron 6276 (9.2)| 384   |
| Palabos [27]                | AMD Opteron 8356 (9.2)| 4     |
| HYPO4D (Groen p.c.)         | BlueGene/P (3.4)      | 512   |
| LBMHD [8]                   | BlueGene/P (3.4)      | 8196  |
| Palabos [27]                | BlueGene/P (3.4)      | 256   |
| MUPHY [28]                  | BlueGene/L (2.8)      | 32    |
| OpenLB [17]                 | Intel Xeon X5550 (10.64)| 8     |
| Palabos [27]                | Intel Xeon X5550 (10.64)| 4     |
| HemeLB (Bifurcation, Sect 4.2) | Xeon E5-2680 (21.6) | 128   |

When a code is not designed for sparse geometries, additional optimisations (e.g., cache lookahead) are simpler to implement, hence the performance of a code which supports sparse geometries may not match that of codes which exploit such optimisations. Many of the benchmarks for other LB codes were performed on non-Opteron architectures, making it difficult if not impossible to do a one-on-one comparison. We nevertheless include these results for reference in the lower part of Table 3.

3. Modelling the performance of HemeLB

3.1. Parameter extraction

Before we are able to construct and apply the performance model, we need to extract a number of parameters specific to HemeLB. These parameters include the maximum neighbour count, the communication volume and the calculation and communication load imbalance.
Table 4: Performance comparison of 12 LB simulations in our code comparison. We provide the name of the LB application used in the first column, followed by the number of lattice sites for each run, the directionality, and the obtained performance per core. We give the per core calculation performance in millions of site updates per second (MSUPS). In the case of LBMHD we assumed 1300 FLOPs per lattice operation, as mentioned in Williams et al. [19, 8]. Runs that use a sparse simulation domain are marked with an asterisk. Three-phase flow runs requires considerably more FLOPs per site update than single-phase flow runs. Here, the OpenLB run used a data set with a fluid fraction of 0.145. The Palabos run on the Opteron relied on shared memory and multi-threading, and did not use MPI.

| Name                      | # of lattice sites | directional resolution | MSUPS per core |
|---------------------------|--------------------|------------------------|----------------|
| HemeLB (Cylinder)         | 15,607,040         | D3Q15                  | 1.41           |
| HemeLB* (Network)         | 18,836,545         | D3Q15                  | 1.20           |
| HemeLB* (Large Network)   | 44,650,496         | D3Q15                  | 1.19           |
| LB3Dv7                    | 16,777,216         | D3Q19                  | 0.30           |
| LB3Dv7 (3-phase flow)     | 56,623,104         | D3Q19                  | 0.084          |
| LBMHD (w/ magnetism)      | 6,115,295,232      | D3Q27                  | 1.42           |
| LBMHD (w/ magnetism)      | 28,311,552,000     | D3Q27                  | 1.15           |
| LUDWIG                    | 339,738,624        | D3Q19                  | 3.0            |
| Palabos (shared memory)   | 64,481,201         | D3Q19                  | 2.55           |
| HYPO4D                    | 452,984,832        | D3Q19                  | 0.273          |
| LBMHD                     | 1,811,939,328      | D3Q27                  | 0.5            |
| Palabos                   | 1,003,003,001      | D3Q19                  | 0.891          |
| LUDWIG                    | 16,777,214         | D3Q19                  | 0.087          |
| MUPHY                     | 262,144            | D3Q19                  | 0.529          |
| OpenLB*                   | 1,060,000          | D3Q19                  | 0.4            |
| Palabos                   | 64,481,201         | D3Q19                  | 7.87           |
| HemeLB* (Bifurcation)     | 19,808,107         | D3Q15                  | 3.49           |

3.1.1. Characterising maximum neighbour count

Each process within HemeLB (except for the steering process) models a subsection of the simulation domain, and exchanges information with its neighbours. Here we characterise the maximum neighbour count ($k_{max}$), which is an approximation of the maximum number of neighbours a process has in a given simulation.

To obtain the neighbour counts of each process, we have run the initialisation routine of HemeLB (without any simulation time steps) using 4 to 16384
Table 5: List of constant values used in our performance model. The $\lambda$ value was measured using a ping test between nodes on HECToR. The $\sigma$ value was taken by dividing the MPI point-to-point bandwidth specification on the HECToR website [29] (at least 5 GB/s) by the number of cores per node (32).

| Constant name | Value                                      |
|---------------|--------------------------------------------|
| $\tau$        | $1.57 \times 10^6$ SUPS per core (calc only) |
| $\lambda$     | $2.5 \times 10^{-5} [s]$                   |
| $\sigma$      | 160 MB/s per core                           |
| $\zeta_{\text{calc}}$ | 1.04                                      |
| $\zeta_{\text{comm}}$ | 1.5                                       |
| $O_{\text{monitoring}}$ | 0.06                                      |

cores. The number of neighbours is dependent not only on core count but also on the geometry of the simulation domain, which makes it non-trivial to fully approximate it in the performance model. Instead, we choose to model close to a worst-case decomposition scenario, selecting the simulation domain with the highest neighbour count, and using the measured values there to determine $k_{\text{max}}$ for any simulation domain. Because ParMETIS does not guarantee a reproducible decomposition, simulations may vary in neighbour counts for a given problem on a given number of cores. We therefore have repeated each measurement three times.

We present our measurements of the maximum neighbour count as a function of the core count in Figure 8. We find that the maximum neighbour count for the network geometry ranges from 7 on 8 cores, up to as high as 94 on 16,384 cores. Based on this data, we created a logarithmic fit, approximating $k_{\text{max}}$ as:

$$k_{\text{max}} = \frac{\log p}{\log 1.127}.$$  

3.1.2. Characterising communication volume

To model the communication performance of HemeLB we also need information on the amount of data communicated between processes at each step. As the domain decomposition in HemeLB is done at runtime [1], we can only know the exact communication data volume after we have launched the simulation. To preserve the predictive power of the performance model, we have instead measured the communication volume for the three types of
simulation domains across a range of core counts. After having performed the measurements, we fitted the data to a function of the form $ax^b$ to gain an approximate estimate while keeping the model relatively straightforward. We present our measurements of the communication volume and our fits for the cylindrical geometries in Figure 9, for the bifurcation geometries in Figure 10, and for the network geometries in Figure 11. Here we find that the communication volume can differ by as much as a factor four between the domain types, making separate fits necessary for each type. We provide the exact formulation for each of the three fits in Table 6. Interestingly, these scale with less than $(N/P)^{2/3}$ as one would expect with, for example, a decomposition into cubes. At large $N/p$, i.e. few processes, the sparseness implies that large parts of the single-process volumes are bordered by boundary sites, rather than lattice sites residing on neighbouring processes.

Figure 8: Maximum number of neighbours as a function of the core count. Here we selected and fitted our model to the Network simulation domain, which has the highest neighbour count due to its sparseness. We ran 3 decomposition routines for each core count included in the figure, plotting the highest neighbour count separately for each instance. The neighbour count approximation used in our performance model is given by the dotted line.
Figure 9: Number of bytes sent per LB simulation step as a function of the number of lattice sites per core for Cylindrical geometries (measurements have been done using the Cylinder simulation domain). The fits we use for Cylindrical, Bifurcation and Network geometries in our performance model are given respectively by the red, blue and black dashed lines. Error bars show one standard deviation for the distribution across cores.

We therefore observe a scaling of less than $(N/P)^{2/3}$. In the limit of small $(N/P)$, the measured communication volume does converge to the function $S = 250 \times (N/P)^{2/3}$ when the number of sites per process becomes lower, and the number of cores used higher in the simulations. Because the process-specific volumes are smaller here, the sparseness of the domain has a smaller effect on the measured (maximum) neighbour count.

3.1.3. Characterising load imbalances

When using sparse geometries, individual processes within HemeLB contain subsets of the simulated system with heterogeneous shapes and sizes. These differences result in two types of load imbalance during the parallel LB calculation: a calculation load imbalance and a communication load imbalance. To obtain a platform-independent measure of the load imbalance in HemeLB, we choose not to include timing results in this procedure. Instead,
we examine the number of lattice sites on each core to determine the calculation imbalance and the number of bytes sent by each process to determine the communication imbalance. Both metrics are reproducible on different platforms when using the same version of ParMETIS (4.0.2), although some variations may occur due to the stochastic nature of the ParMETIS decomposition technique.

In Fig. 12 we show the measured calculation load imbalance for three geometries as a function of the core count. We determine this calculation load imbalance by dividing the maximum number of lattice sites on any core within this run by the average number of sites over all cores in the same run. HemeLB is optimised for calculation load balance and we find an imbalance of less than 1.04 for most core counts. However, the calculation load imbalance is higher for both very low and very high core counts. This contributes in part to the superlinear scaling of HemeLB at lower core counts in some cases, and reduces scalability when there are less than 2000 lattice sites per core. Based on these measurements, we assume a calculation load imbalance ($\zeta_{\text{calc}}$)
of 1.04 in our performance model.

In Fig. 13, we present the *communication load imbalance*, which we measure by dividing the maximum number of bytes sent by a single core in the run by the average number of bytes sent per core. All the communication measurements are given per step. We observe a large and erratic imbalance in the communication sizes. The ParMETIS domain distribution algorithm co-optimizes for both calculation load balance and communication minimisation. However, these results suggest that it does not optimize for communication balance. This communication imbalance does not strongly diminish the code performance unless the performance is already dominated by communication. Within our model we take an approximate average of our measurements, and assume a communication load imbalance \( \zeta_{\text{comm}} \) of 1.5.
Table 6: List of fitting functions used in our performance model. Here the total number of lattice sites is given by $N$ and the number of cores used by $p$.

| Constant name   | Value                                                                 |
|-----------------|----------------------------------------------------------------------|
| $S_{\text{cylinder}}$ | $1898 \times (N/p)^{0.482719}$ bytes per core per step          |
| $S_{\text{bifurcation}}$ | $942.0 \times (N/p)^{0.595517}$ bytes per core per step         |
| $S_{\text{network}}$    | $1176 \times (N/p)^{0.613449}$ bytes per core per step          |

Figure 12: Imbalance of the number of sites per core (i.e., our measure for calculation load imbalance) as a function of the number of cores for the three geometries. The value on the y-axis is the relative calculation overhead caused by load imbalance. These values are deterministic for a given core count and ParMETIS version.

3.2. LB calculations

To model the performance of the core LB simulator code we propose a time-complexity model which is loosely based on [22, 23] but largely simplified. We use a range of parameters which we derived in Section 3.1. In this model we approximate the overall time spent to perform a single simulation step in HemeLB ($T_{\text{step}}$), using
Communication load imbalance

Figure 13: Imbalance in the number of bytes sent (i.e., our measure for communication load imbalance) as a function of the number of cores for the three geometries. The value on the y-axis is the relative communication overhead caused by load imbalance. These values are deterministic for a given core count and ParMETIS version.

\[ T_{\text{step}} = \frac{\zeta_{\text{calc}} \times T_{\text{calc}} + \zeta_{\text{comm}} \times T_{\text{comm}}}{1.0 - O_{\text{monitoring}}}, \]

where \( T_{\text{calc}} \) is the average calculation time per core, \( (\zeta_{\text{calc}}) \) is the calculation load imbalance constant, \( T_{\text{comm}} \) is the communication time per core, \( \zeta_{\text{comm}} \) is the communication load imbalance constant and \( O_{\text{monitoring}} \) is the fraction of time spent on monitoring overhead. Throughout our runs we found that \( \sim 6\% \) of the runtime is spent on monitoring, so we define \( O_{\text{monitoring}} = 0.06 \).

The average calculation time per core is given by

\[ T_{\text{calc}} = \frac{(N/p)}{\tau} \]

Here, the total number of lattice sites is given by \( N \) and the number of cores by \( p \). We define the SUPS per core \( \tau \) as a platform dependent constant for
the HECToR machine in Table [5]. We measured $\tau$ as an average from our HemeLB runs with 32 cores (1 node). The true SUPS capacity per core depends slightly on the number of sites per core, but is in almost all cases within 20% of this average value. We model the time spent on communications, $T_{\text{comm}}$, using

$$T_{\text{comm}} = \log_2(p) \times \lambda + \frac{S_{\text{<xx>}}}{\sigma},$$

where $\lambda$ is the point-to-point latency of MPI communications between nodes in seconds, and $\sigma$ the average throughput capacity per core in bytes. We assume that the number of messages exchanged per time step increases with the number of processes and we model this as $\log(p)$. The number of bytes sent out per core per step ($S_{\text{<xx>}}$) is dependent on the geometry used as well as the number of sites per core. We have provided basic fits for three geometry layouts with different sparsity (network, bifurcation and cylinder) in Table [5]. These fits are most accurate for simulations that have between 5,000 and 200,000 sites per core.

### 3.3. Visualisation

When image rendering and writing is enabled in HemeLB, some overhead is introduced in the execution, and the new time per step ($T_{\text{step,vis}}$) becomes

$$T_{\text{step,vis}} = T_{\text{step}} + T_{\text{images}},$$

where $T_{\text{images}}$ is the overhead for rendering and writing images. Because our overhead measurements show a large variability, we use a straightforward fit rather than a detailed sub-model to approximate this overhead. Based on our measurements on 2048 cores, we have derived an approximate fit of $T_{\text{images}} = 21.6k^{-0.76}$, with $k$ being the number of LB steps per rendered image. We provide a graphical overview of the approximation in Figure [6].

### 4. Model validation

#### 4.1. Validation on HECToR

We have applied our performance model to calculate the theoretical execution times of the simulations we presented in Section [2.1]. The predictions
Figure 14: Wall-clock time spent to simulate 100 time steps as a function of the number of cores used for the Cylinder, Bifurcation and Large Bifurcation simulation domains. These validation runs were done using the HECToR supercomputer. Predictions by our performance model are indicated by the dashed lines.

given by the model, as well as the measurements presented earlier, can be found in Figure 14 for the Cylinder, Bifurcation and Large Bifurcation simulation domains and in Figure 15 for the Network, Small Network and Large Network simulation domains. The predictions from our model are generally in agreement with our measurements, especially for the larger simulation domains. However, the model does not reproduce the superlinear speedup measured in the results. This is mainly because the model assumes a constant calculation and communication load imbalance, regardless of core count. In contract we measure relatively large calculation and communication load imbalances for runs on less than 32 cores (see Figures 12 and 13). In this regime, the measured load imbalances are considerably higher than the ones assumed in our model, and the execution time is consequently slightly higher than in our model predictions.
4.2. Validation on SuperMUC

To test whether our performance model holds when applied to a different platform, we used a small part of an allocation arranged by MAPPER on the SuperMUC supercomputer at the Leibniz-Rechenzentrum in Garching, Germany. SuperMUC is an IBM System x iDataPlex machine with 147456 compute cores and a total peak performance of 3.185 PFLOP/s (21.6 GFLOP/s per core). Each node has 16 cores, consists of two Intel Xeon E5-2680 CPUs, and is equipped with 32 GB of memory. The nodes are interconnected with an Infiniband FDR10 network, which divides the supercomputer into islands, each of which contains 8192 cores. We use this machine to run HemeLB simulations using the Bifurcation simulation domain, and to compare our measurements to our model predictions. We provide the list of constant values in Table 7. The values of $\zeta_{\text{calc}}$, $\zeta_{\text{comm}}$ and $O_{\text{monitoring}}$ are the same as those we used for HECToR, as these constants do not depend on the underlying architecture. We obtained a $\sigma$ value of 500 MB/s per core through direct
Table 7: List of constant values used in our performance model for SuperMUC. The $\lambda$ value was measured using a ping test between nodes on SuperMUC. The $\sigma$ value was taken by dividing the MPI point-to-point bandwidth specification on the SuperMUC website [29] (at least 5 GB/s) by the number of cores per node (16).

| Constant name | Value                        |
|---------------|------------------------------|
| $\tau$       | $4.2 \times 10^6$ SUPS per core (calc only) |
| $\lambda$    | $1.83 \times 10^{-4}$[s]    |
| $\sigma$     | 500 MB/s per core            |

correspondence with LRZ, and measured a $\lambda$ of $1.83 \times 10^{-4}$ s by running a ping job between two nodes within the same island, and taking the average from 10 pings. As all small jobs on SuperMUC tend to get scheduled on the same island, it was unfortunately not possible to accurately measure the latency between islands. We obtained the value of $\tau$ by running a very short HemeLB simulation on one node and extracting the calculation rate per core, excluding any communications or other overhead ($4.2 \times 10^6$ SUPS).

We present both our model predictions and our performance measurements in Figure 16. Here we find that our simulation runs considerably faster on SuperMUC than on HECToR, achieving 3.49 MSUPS per core when using 128 cores, and 3.00 MSUPS per core when using 2048 cores. Our performance model accurately predicts the runtime for simulations up to 4096 cores, and matches the measured performance even more closely than in the HECToR validation tests. We have performed 2 runs using 8192 cores, one using one island, and on distributed over two islands. Our performance model predicts a time which is higher than the measured time for the single-island run. This may be because the ping test we used over the Infiniband has given us a somewhat higher $\lambda$ than the actual point-to-point latency of communications in the MPI layer. Communications between islands experience much higher latency and lower bandwidth (at a 4:1 ratio). As a result, the run performed using two islands is an order of magnitude slower slower than the run using one island. Understanding the performance across islands would require us to assess the latency and bandwidth characteristics of the inter-island links (which would require a special access mode), and incorporate these in a separate "inter-island" set of the parameters $\lambda$ and $\sigma$. 

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5. Discussion

We have presented a range of performance measurements for HemeLB, covering the lattice Boltzmann simulation and the visualisation and steering functionalities. For the models studied here, HemeLB scales near-linearly up to 32,768 cores, even for highly sparse simulation domains such as vascular networks. The application achieves close to maximum efficiency when using between 5,000 and 500,000 lattice sites per core. We have shown that HemeLB can render and write images once every 100 timesteps with an overhead of $\sim$10%, sharing streaming images and control with a steering client at 4.6 fps with a 28% overhead. We have demonstrated that it is possible to create a model which can estimate the run time of HemeLB simulations in advance. In our validation tests, we find that the predictions are between 70% and 140% of the actual runtime for simulations with at least 5000 lattice sites per core, and that our model remains largely accurate when applied to a different architecture (SuperMUC). We believe that accurate runtime
predictions will be useful in the long term when HemeLB is used in a clinical setting, as doctors will be able to select the simulation with the highest accuracy that still meets the deadline for actual treatment.

To improve the accuracy of HemeLB simulations, as part of the MAPPER project [30], we have developed an intercommunication layer that allows the code to exchange boundary information with other simulation codes [31]. These couplings allow us to incorporate phenomena that are not resolved in HemeLB itself, such as the interaction between the blood flow in the intracranial vasculature and that in the rest of the human body. The boundary exchanges in these coupled simulations occur at high frequency and require rapid response times on both ends. The performance bottlenecks we have identified allow us to take the necessary steps to ensure an optimal performance for multiscale simulations using HemeLB.

The envisaged use-case for HemeLB, involving deployment within a clinical setting, is made more difficult by typical queueing and scheduling policies for supercomputers. One important benefit of supercomputing lies in enabling results to be produced in a timely fashion. With typical scheduling policies, however, many codes produce results only after a lengthy wait in a queuing system, significantly reducing the value-added of the supercomputing resource relative to a long-running simulation on a smaller machine. The value of supercomputing is particularly apparent when using interactive visualisation and steering [2], as this enables complex simulations to be investigated on timescales close to those of human engagement. However, this form of interaction is not possible without an advance reservation facility, enabling one to predict the time when one will be able to interact with the running simulation.

In particular, in the clinical context, patients and physicians already interact within a complex resource availability and scheduling environment. In this case, advance reservation will be necessary to make computing resources available concurrently with medical equipment, physicians, and patient needs. Furthermore, when HemeLB is used in a clinical context, rapid access to computing resources will become a safety-critical factor. This requires not just advance reservation, but support for urgent computing [3].

For the use cases we envisage for HemeLB, an urgent computing mechanism will need to be available on supercomputing resources.
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