A SURVEY OF THE MOLECULAR ISM PROPERTIES OF NEARBY GALAXIES USING THE HERSHEY FTS

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ABSTRACT

The 12CO J = 4 → 3 to J = 13 → 12 lines of the interstellar medium from nearby galaxies, newly observable with the Herschel SPIRE Fourier transform spectrometer, offer an opportunity to study warmer, more luminous molecular gas than that traced by 12CO J = 1 → 0. Here we present a survey of 17 nearby infrared-luminous galaxy systems (21 pointings). In addition to photometric modeling of dust, we modeled full 12CO spectral line energy distributions from J = 1 → 0 to J = 13 → 12 with two components of warm and cool CO gas, and included LTE analysis of [C i], [C ii], [N ii], and H2 lines. CO is emitted from a low-pressure/high-mass component traced by the low-J lines and a high-pressure/low-mass component that dominates the luminosity. We found that, on average, the ratios of the warm/cool pressure, mass, and 12CO luminosity are 60 ± 30, 0.11 ± 0.02, and 15.6 ± 2.7. The gas-to-dust-mass ratios are <120 throughout the sample. The 12CO luminosity is dominated by the high-J lines and is 4 × 10^{-4} L_{FIR} on average. We discuss systematic effects of single-component and multi-component CO modeling (e.g., single-component J ≤ 3 models overestimate gas pressure by ~0.5 dex), as well as compare to Galactic star-forming regions. With this comparison, we show the molecular interstellar medium of starburst galaxies is not simply an ensemble of Galactic-type giant molecular clouds. The warm gas emission is likely dominated by regions resembling the warm extended cloud of Sgr B2.

Key words: galaxies: ISM – ISM: molecules – submillimeter: general

Online-only material: color figures

1. INTRODUCTION

Cool molecular gas in the interstellar medium (ISM) is the raw material out of which stars will form. The carbon monoxide molecule (12CO, henceforth CO) is known to be an excellent tracer of the total molecular hydrogen in the ISM, especially at the ground-state rotational transition of J = 1 → 0. For many prominent nearby galaxies, such as M82, Arp 220, and NGC 1068, the emission from the higher-J lines of CO has proven to be far more luminous than would have been predicted from ground-based observations restricted to low-J lines (e.g., Panuzzo et al. 2010; Kamenetzky et al. 2012; Rangwala et al. 2011; Spinoglio et al. 2012; Rigopoulou et al. 2013; Pereira-Santaella et al. 2013). It is already well established that the ISM is comprised of a multitude of constituents, both in composition (ionized, atomic, molecular) and physical conditions (temperatures, densities). High-J lines of CO offer a new opportunity to study the relatively warm (compared to low-J CO), yet still molecular, ISM. This warmer CO is notable because of its much larger luminosity, representing a much greater role in the total energy budget of the molecular gas. Therefore, to study the ongoing questions regarding the feedback interactions between different energy sources (cosmic rays, ultraviolet light from stars, X-rays from active galactic nuclei (AGNs), or mechanical heating from turbulence, winds, shocks, etc.), one must specifically examine the warmer CO via high-J transitions.

In general, due to atmospheric water absorption, only the lowest-J lines of CO can be observed from the ground. However, the launch of the Herschel Space Observatory (Pilbratt et al. 2010) offered a unique opportunity to observe at higher frequencies. The Spectral and Photometric Imaging REceiver (SPIRE) instrument (Griffin et al. 2010) consisted of a three-band imaging photometer and an imaging Fourier transform spectrometer (FTS). The FTS simultaneously observed spectra from 447–1550 GHz, which for nearby galaxies, encompasses the 12CO J = 4 → 3 to J = 13 → 12 transitions, among other molecular and atomic fine structure lines.

Herschel’s mission has come to an end because of its finite supply of cryogens, but it has left behind an impressive legacy of observations. Approximately 300 galaxies have been observed in point-source mode with the FTS, with spectra of varying quality. In this paper, we establish a uniform pipeline for analysis of FTS spectra of galaxies, from the raw observations to the determination of the physical parameters of the cool and warm emitting CO gas. We present initial results for 21 pointings of 17 unique galaxy systems, most of which have been well studied in the past. The motivation for this survey is to understand the physical parameters (e.g., pressure and mass) that describe warm CO emission and to determine how the parameters vary with galaxy type, total infrared luminosity, etc. We sought to answer many questions brought to light by this new data. Is the highly luminous warm component of molecular gas found in early Herschel SPIRE FTS studies generically present in high star-formation rate (SFR) galaxies, and how does its presence modify what we already knew about cool molecular gas? Given the broad range of CO lines we now have with Herschel, can we reassess the CO luminosity to mass conversion factor, and dust-to-gas mass ratios? Accounting for the warm gas component luminosities, what L_{CO}/L_{FIR} are observed, and what other

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3 Herschel is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.
properties vary with, e.g., $L_{\text{FIR}}$? What are the relative column densities of C\textsuperscript{+}, C, and CO in nearby starburst galaxies; in other words, where is the carbon not locked up in grains? Finally, how do the molecular gas pressures of the galaxies in our sample compare to Galactic giant molecular clouds? Studying the physical parameters of the gas provides necessary information to interpret the energy budget and physical processes acting on the gas. Additionally, it informs the analysis of high-redshift galaxies with fewer observed lines. This paper represents a sub-sample of a planned archival study of the molecular gas and dust in as many galaxies as possible observed with the FTS.

Section 2 describes how the Herschel observations were utilized, including sample selection, source–beam coupling correction and spectral line fitting. Section 3 details our modeling methodology: dust and CO likelihood analysis with Multinest (Feroz et al. 2009), and LTE analysis of H\textsubscript{2}, [C\textsc{ii}], [C\textsc{iii}], and [N\textsc{ii}]. A flowchart in Figure 1 should help the reader understand the many types of data and modeling utilized in this work. Section 4 summarizes our findings for this sample of galaxies, including a discussion of systematic effects of two-component likelihood modeling of physical properties, the calculation of the CO luminosity-to-mass conversion factor and gas-to-dust mass, and comparisons among our galaxies and Galactic star-forming regions. Finally, we present conclusions and future plans in Section 5.

2. OBSERVATIONS

2.1. Sample Selection

This paper utilizes publicly available data from both the SPIRE spectrometer (FTS) and photometer, downloaded from the Herschel Science Archive. The 21 pointings in Table 1 represent 17 unique galaxy systems. This table lists both the observation IDs, coordinates and some basic properties of the sample galaxies; they are presented in order by R.A. in this table only, and will subsequently be presented in order of far-infrared luminosity, $L_{\text{FIR}}$ (the last column, “Order,” can help the reader find each galaxy in subsequent tables and figures). Some of the interacting galaxies with separated nuclei had FTS observations centered at each nucleus: there are two separate pointings within the Antennae (NGC 4038 and the Overlap region), two within NGC 1365, and three within Arp 299. Appendix A includes additional information on how these and other extended galaxies were handled.

These specific galaxies were chosen because they are relatively nearby (10 within 50 Mpc, all within $\sim$260 Mpc) and their spectra showed measurable, bright CO emission. Six are identified as AGNs (UGC 05101, NGC 1068, Cen A, NGC 1365, Mrk 273, Mrk 231), three as ULIRGS (Arp 220,

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4 Throughout this work, we use $L_{\text{FIR}}$ to refer to the integrated flux from 8–1000 $\mu$m; definitions vary in the literature.
The SPIRE photometer bands are 250, 350, and 500 μm. The FTS contains two arrays of detectors: the lowest frequencies are captured by the spectrometer long wave (SLW; 303–671 μm) and the higher frequencies by the spectrometer short wave (SFW; 52–523 μm). The calibration of the FTS is done in two steps: (1) we use a spectrally resolved point source and convolve its spectrum, scaled to the FTS frequency sampling, to the FTS PSW beam shape and determine the flux density scaling factor; and (2) we convolve this PSW flux density to the beam of the chosen FTS line. The FTS measured the total flux in Jy at all wavelengths. For a uniformly extended source (Ωₜ ≪ Ωₑ), the flux density scaled with Ωₑ, i.e., \( F_{\text{TS}} / F_{\Omega} \), \( \Omegaₜ/Ωₑ \), will be normalized by that convolved to \( \Omegaₜ \) line. To determine \( \Omegaₜ/Ωₑ \), we convolve the PSW map with a Gaussian kernel of size \( \Omegaₜ/Ωₑ \). Many of the sources in this sample are semi-extended, meaning their source size is comparable to the beam size of the FTS. In this case, \( (Fₜ/Fₜ) = \eta₁₂ \), where \( \eta₁₂ \) will be between \( \Omegaₜ/Ωₑ \) (uniform extended) and 1 (point source). We use a two-step procedure to correct the spectra for source-beam coupling effects: (1) derive \( \eta₁₂ \) from photometry maps and use it to scale all fluxes to a 43″ beam (that of the CO \( J = 4 \rightarrow 3 \) line), and (2) scale the resulting spectrum to match the total photometer fluxes. The final spectrum is as if it were observed by an instrument with a constant beam size.

Proper modeling of \( \eta₁₂ \) is necessary to compare flux densities measured at different frequencies of the FTS band as well as those measured from other telescopes. For this we follow a similar procedure to that used in Panuzzo et al. (2010) using the PSW (250 μm) maps. Because \( \Omegaₜ/Ωₑ \) is \( \sim 45'' \) to \( 17'' \) across both bands (\( \Omegaₑ = 1.133 b^2 \)), for a point source (\( \Omegaₑ \gg Ωₜ \)), the FTS measured the total flux in Jy at all wavelengths. For a uniformly extended source (\( Ωₑ \ll Ωₜ \)), the flux density scaled with \( Ωₑ \), i.e., \( Fₜ/Ωₜ \), will be normalized by that convolved to \( Ωₑ \) line.

### 2.2. Source–Beam Correction of Semi-extended Sources

The emission we measured in the FTS (\( Fₜ \)) was produced by the multiplication of the (generally non-Gaussian) source and beam. The beam size, \( \Omegaₜ \), varied from \( b \) (effective Gaussian FWHM) \( \sim 45'' \) to \( 17'' \) across both bands (\( \Omegaₑ = 1.133 b^2 \)). For a point source (\( \Omegaₑ \gg Ωₜ \)), the FTS measured the total flux in Jy at all wavelengths. For a uniformly extended source (\( \Omegaₑ \ll Ωₜ \)), the flux density scaled with \( Ωₑ \), i.e., \( Fₜ / Ωₜ \), \( Ωₑ / Ωₜ \), will be normalized by that convolved to \( Ωₑ \) line. Many of the sources in this sample are semi-extended, meaning their source size is comparable to the beam size of the FTS. In this case, \( (Fₜ / Ωₑ) \) will be between \( Ωₑ / Ωₜ \) (uniform extended) and 1 (point source). We use a two-step procedure to correct the spectra for source-beam coupling effects: (1) derive \( η₁₂ \) from photometry maps and use it to scale all fluxes to a 43″ beam (that of the CO \( J = 4 \rightarrow 3 \) line), and (2) scale the resulting spectrum to match the total photometer fluxes. The final spectrum is as if it were observed by an instrument with a constant beam size.

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Table 2  
Source/Beam Correction Parameters

| FTS Name | $\eta(15, 43.5) = a + b\Omega + c\Omega^2 + d\Omega^3$ | $\eta(15, 43.5)$ |
|----------|---------------------------------|-----------------|
|          | $a \times 10^1$ | $b \times 10^2$ | $c \times 10^4$ | $d \times 10^6$ |
| Mrk 231  | 7.3               | 1.3             | -2.4            | 1.9               | 0.88            |
| IRAS F17207-0014 | 8.1          | 0.92            | -1.8            | 1.5               | 0.91            |
| IRAS 09022-3615 | 7.0           | 1.6             | -2.9            | 2.1               | 0.88            |
| Arp 220  | 6.6               | 1.6             | -2.9            | 2.2               | 0.85            |
| Mrk 273  | 7.8               | 1.1             | -2.0            | 1.7               | 0.90            |
| UGC 05101 | 8.2           | 0.88            | -1.7            | 1.5               | 0.92            |
| NGC 6240 | 4.3               | 2.5             | -4.0            | 2.7               | 0.73            |
| Arp 299-C | -3.7             | 4.7             | -4.6            | 2.1               | 0.25            |
| Arp 299-B | -4.0              | 4.7             | -4.1            | 1.7               | 0.21            |
| Arp 299-A | 0.45              | 3.8             | -4.9            | 2.9               | 0.51            |
| NGC 1068 | -4.7              | 5.7             | -7.3            | 4.2               | 0.24            |
| NGC 1365-SW | -4.7          | 5.8             | -7.4            | 4.2               | 0.25            |
| NGC 1365-NE | -0.042          | 4.4             | -6.6            | 4.1               | 0.52            |
| NGC 4038 | 1.8               | 0.54            | 3.7             | -1.4              | 0.34            |
| NGC 4038 (Overlap) | -2.7         | 4.3             | -4.6            | 3.4               | 0.28            |
| M82      | -2.9              | 5.2             | -6.9            | 4.1               | 0.35            |
| NGC 1222 | 1.3               | 3.9             | -4.1            | 3.8               | 0.60            |
| M83      | -1.7              | 4.4             | -5.4            | 3.6               | 0.38            |
| NGC 253  | 1.9               | 3.4             | -5.0            | 3.5               | 0.60            |
| NGC 1266 | 5.2               | 2.3             | -3.8            | 2.7               | 0.78            |
| Cen A    | -0.012            | 2.2             | -0.34           | 1.2               | 0.33            |

find $\eta(\Omega_6, \Omega_{43.5})$ for various beams from 20 to 43 arcsec. We fit the resultant curve as a third order polynomial, the parameters for which are given in Table 2. The last column shows $\eta_{15, 43.5}$ as an example. For M82, a telescope with a 15′ beam (pointed at the same location as the FTS) would only measure 35% of the emission measured in a 43.5 beam. UGC 05101, in contrast, is extremely point-like; a 15′ beam would measure 91% of the flux despite having only 12% of the beam area. Knowing the beam size at each frequency, we divide the entire spectrum by the appropriate $\eta(v)$ for those galaxies whose $\eta_{20,43.5}$ is less than 90% (where we expect to be measuring real signal above a conservative 10% calibration error). This step removes the discontinuity between SLW and SSW, which indicates that we have correctly stitched together the flux over the discontinuity in beam sizes.

The second step is an additional calibration to match the absolute flux to that of the SPIRE photometer maps. We convolve each map by a kernel $\Omega_{\text{kernel}} = \Omega_{43.5} - \Omega_{\text{phot}}$ to match 43.5. $\Omega_{\text{phot}}$ is 423, 751, and 1587 arcsec$^2$ for PSW, PMW, and PLW, respectively. We then measure the flux in Jy beam$^{-1, 43.5}$ at the point where the FTS beam is pointing, which is $F'(\text{PSW})$, for example. We compare this flux to that from the FTS spectrum ($S(v)$), considering the (unweighted) photometer response function, $R(v)$, which is $\tilde{F}(S(v))$. We then multiply by the ratio $X_{\text{SSW}} = F''(\text{PSW})/F'(\text{PSW})$. There are two photometer bands (PMW and PLW) that overlap with the SSW band, so we define a line that connects those two ratios, thus dividing by $X_{\text{SLW}}(v)$. Often, the first step ($\eta$) overestimates the total flux in the SSW especially, and the second step (absolute flux calibration) reduces the overestimation, and can result in lower spectra (e.g., NGC 1222, NGC 1266).

Therefore the final corrected spectrum for SLW/SSW is $F_i(v) = \frac{X_{\text{SLW/SSW}}F'(v)}{\eta(v)}$. The spectra are shown in Figures 2, 3, and 4. The empirical fits for $\eta(\Omega_6, \Omega_{43.5})$ from Table 2 were also used to correct fluxes from the literature for CO modeling (see Section 3.2.1).

2.3. FTS Spectral Line Fitting

To fit the CO, [C\text{i}], and [N\text{ii}] lines, we used the FTfitter code from the University of Lethbridge. Some of our spectra contain many more lines (for example, Arp 220, Rangwala et al. 2011), but we do not fit them here in the interest of establishing a consistent pipeline for the brightest lines in all galaxies. For one detector (SLW or SSW) at a time, we first determine a polynomial fit to the baseline and then fit unresolved lines at the expected frequencies given the known redshifts. The code utilizes the instrumental line profile to determine the area underneath each line in Jy cm$^{-1}$.

Most of the lines in this sample are unresolved; however, the velocity resolution improves at the highest frequencies, and the highest-J CO lines and [N\text{ii}] line are sometimes resolved. These lines do not show the characteristic ringing of the sinc function, which is the expected line profile for an FTS. By visual inspection, we determined which lines were clearly resolved and refit them as a Gaussian convolved with the instrumental line profile. Though the code cannot break the degeneracy between the Gaussian amplitude and width, the area is well constrained. The [N\text{ii}] line, the highest frequency line in our spectrum, was resolved in the following 11 galaxies: UGC 05101, NGC 1068, Arp 220, Mrk 273, Mrk 231, NGC 6240, Arp 299-A, -B, -C, NGC 1266, and IRAS 09022-3615. Two of these galaxies showed resolved line structure for multiple lines. All lines at and above CO $J = 9 \rightarrow 8$ were resolved for Mrk 273, and all lines at and above CO $J = 6 \rightarrow 5$ were resolved for NGC 6240. Additionally, the CO $J = 7 \rightarrow 6$ and [C\text{i}] $J = 2 \rightarrow 1$ lines are very close to one another; for three of the spectra (UGC 05101, Cen A, Arp 220), we manually fitted variable-width sinc functions to the lines when the FTfitter code could not properly fit the two.

The integrated fluxes are shown in Tables 3, 4, and 5. Our most luminous galaxies are distant enough that the CO $J = 4 \rightarrow 3$ line is either completely redshifted out of the band, or extremely close to the edge. Fluxes are not reported in those cases.

In Figure 5, we show the CO spectral line energy distributions (SLEDs), all scaled such that the luminosity of $J = 1 \rightarrow 0$ line matches that of Mrk 231 (see Section 3.2.1 for how the low-J line fluxes were acquired from the literature). This figure illustrates just how varied the shapes of the CO SLEDs become at higher-$J$, and includes comparisons to Galactic sources, which will be discussed in Section 4.6.

2.4. Photometry

In addition to using the SPIRE photometry maps to determine the source–beam coupling correction, we also performed aperture photometry to obtain galaxy-integrated fluxes to supplement the dust modeling. Results are in Table 6. A circular aperture was centered on the FTS pointing location of the dust map, and a radius ($r_a$) was chosen to encompass all of the measured flux. The sky background is calculated from an annulus with inner radius $r_a$ to outer radius $r_a + 10$ pixels. The sky is calculated as the median value of the data (Jy beam$^{-1}$) divided by (beam pixel$^{-1}$) times the area contained in the annulus (in pixels). For all points within $r_a$, the flux is the total of the data divided by beam pixel$^{-1}$ minus the sky.

6 https://www.uleth.ca/phy/naylor/index.php?page=ftfitter
Figure 2. Source–beam coupling corrected FTS spectra 1 of three. The galaxies, starting with this figure, are in order of decreasing far-infrared luminosity. The uncorrected spectra are shown in gray, the corrected spectra (as described in Section 2.2) are plotted over top in black. For point-source-like spectra, e.g., UGC 05101, the correction may be unnoticeable. The redshifted locations of the $^{12}$CO, [C\textsc{i}], and [N\textsc{ii}] lines are shown with dotted, dashed, and dash-dotted lines, respectively.
Figure 3. Source–beam coupling corrected FTS spectra 2 of three. See Figure 2 caption for more information.
Figure 4. Source–beam coupling corrected FTS spectra 3 of three. See Figure 2 caption for more information.
For both dust and CO modeling, we utilize the nested sampling algorithm MultiNest (Feroz et al. 2009) and its Python wrapper, PyMultiNest (Buchner et al. 2014). As stated in Feroz et al. (2009), nested sampling “is a Monte Carlo technique aimed at efficient evaluation of the Bayesian evidence, but also produces posterior inferences as a by-product.” The evidence in this context is the average likelihood of a model over its prior probability space. The algorithm “nests inward” to subsequently smaller regions of high-likelihood parameter space. Unlike calculating the likelihood using a grid method, the algorithm can focus on high likelihood regions and thus estimate parameter constraints more efficiently.

In both cases (dust and CO), described in their respective sections (Sections 3.1 and 3.2), we have a set of measurements \( x \) with errors \( \sigma \), a model described by parameters \( p \) with predicted fluxes \( I(p) \). For a Gaussian probability, the natural log of the likelihood is

\[
\ln p \propto -\frac{1}{2} \sum_i (x_i - I(p)) \sigma_i^{-2} \ln(\sigma_i) - \frac{1}{2} \frac{(x_i - I(p))^2}{\sigma_i^{-2}}
\]

The covariance matrix is fully described for the dust modeling in Section 3.1. For the CO modeling, we use zero covariance between data points, simplifying the probability to

\[
\ln p \propto -\frac{1}{2} \sum_i (x_i - I(p))^2 \sigma_i^{-2}
\]

This is used in the plots of best-fit spectral (line) energy distributions, but we focus our discussion on the marginalized likelihoods.

In the case of a complicated parameter space, there can be multiple “modes,” or islands in parameter space, as was sometimes the case for the CO modeling. The MultiNest algorithm partitions the posterior likelihood space into ellipsoids, which may overlap. Non-overlapping ellipsoids can be separated into separate modes, with a separate “local” evidence. In our cases, all posterior distributions with multiple likelihoods had one mode stand out as containing more posterior mass than others; we focus our parameter estimation on this most-likely mode, as opposed to the mean that one would calculate considering the entire posterior distribution, which would be weighted toward other, less-likely modes. The extent of that weighting would depend on the ratio of the different local evidence.

### 3.1. Dust Modeling Likelihood with Multinest

We can determine the probability distribution for any one parameter by marginalizing the full distribution over all other parameters. There are different statistics that can be used to describe a parameter. The best-fit set of parameters is the combination that produced the highest likelihood. In the case of a very simple parameter space, where the solution is clustered in a Gaussian fashion in one area, the best-fit will likely coincide with the statistical mean of each parameter. This was the case for the dust modeling. However, the parameter space may not be so simply described, which we will demonstrate for the CO modeling. This mode of parameter estimation is designed to focus on the whole probability density function (PDF), not to refine the best fit. We present the best-fit in our tables, as it is used in the plots of best-fit spectral (line) energy distributions, but we focus our discussion on the marginalized likelihoods.

In addition to SPIRE photometer observations (250, 350, 500 \( \mu \)m), we also used fluxes from the literature, those listed in Tables 7–13 above 10 \( \mu \)m. These are galaxy-integrated fluxes; we only modeled once per galaxy with multiple FTS pointings.
Table 4
Integrated Fluxes in 10^2 Jy km s^{-1}: CO, Continued

| FTS Name  | \( J = 9 \rightarrow 8 \) | \( J = 10 \rightarrow 9 \) | \( J = 11 \rightarrow 10 \) | \( J = 12 \rightarrow 11 \) | \( J = 13 \rightarrow 12 \) |
|-----------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Mrk 231   | 5.00 0.48       | 6.53 0.35       | 5.14 0.33       | 3.80 0.27       | 3.31 0.27       |
| IRAS F17207-0014 | 9.45 0.87 | 9.04 0.53 | 4.77 0.57 | 2.39 0.45 | 1.65 0.44 |
| IRAS 09022-3615  | 6.27 0.50  | 4.11 0.30  | 2.80 0.28  | 2.45 0.27  | 1.42 0.24  |
| Arp 220    | 25.6 2.6     | 24.4 2.1     | 12.6 2.2     | 7.23 1.8     | 5.47 1.7     |
| Mrk 273   | 7.85 0.95    | 9.33 0.68    | 4.19 0.67    | 4.23 0.65    | 4.42 0.66    |
| UGC 05101 | 2.51 0.45    | 3.08 0.31    | 2.13 0.34    | 0.734 0.27   | 1.10 0.25    |
| NGC 6240  | 49.2 1.3     | 43.5 0.92    | 31.2 0.95    | 24.4 0.78    | 20.2 0.81    |
| Arp 299-C | 9.20 0.60    | 5.74 0.48    | 3.93 0.49    | 4.79 0.41    | 3.15 0.40    |
| Arp 299-B | 8.15 0.60    | 5.85 0.49    | 4.15 0.46    | 5.88 0.42    | 4.41 0.43    |
| Arp 299-A | 24.5 0.78    | 19.8 0.71    | 14.2 0.69    | 13.6 0.60    | 10.8 0.64    |
| NGC 1068  | 75.2 2.5     | 69.1 2.2     | 56.8 2.1     | 50.8 2.0     | 27.7 2.1     |
| NGC 1365-SW | 15.3 1.6   | 10.2 1.5     | 4.83 1.5     | 3.94 1.3     | ...          |
| NGC 1365-NE | 16.6 1.6  | 6.58 1.5     | 7.13 1.3     | 4.33 1.0     | 5.52 1.4     |
| NGC 4038  | 2.30 1.2     | 3.52 0.93    | 1.46 0.99    | 3.36 0.89    | 3.29 0.97    |
| NGC 4038 (Overlap) | 6.68 1.3 | 3.58 1.4    | ...          | ...          | ...          |
| M82       | 394 6.4      | 289 6.9      | 188 7.6      | 136 6.4      | 88.1 6.2     |
| IRG 1222  | 1.56 0.40    | 0.861 0.38   | 1.02 0.37    | 0.277 0.29   | 1.05 0.33    |
| M83       | 21.8 2.7     | 10.0 2.7     | 11.4 2.8     | ...          | ...          |
| NGC 253   | 416 11       | 291 12       | 216 14       | 155 15       | 91.3 17      |
| NGC 1266  | 11.9 0.48    | 9.62 0.42    | 7.47 0.41    | 6.32 0.36    | 4.35 0.38    |
| Cen A     | 9.20 1.2     | 5.81 1.1     | 2.13 1.2     | 2.90 0.97    | 5.62 1.2     |

Note. See Table 3 for more information.

Table 5
Integrated Fluxes in 10^2 Jy km s^{-1}: [C\text{\textit{i}}] and [N\text{\textit{ii}}]

| FTS Name  | [C\text{\textit{i}}] 1–0 | [C\text{\textit{i}}] 2–1 | [N\text{\textit{ii}}] |
|-----------|-----------------|-----------------|-----------------|
| Mrk 231   | \( I_{\Delta v} \) | \( I_{\Delta v} \) | 5.00 0.30       | 6.42 0.83       |
| IRAS F17207-0014 | 6.17 1.9 | 6.68 0.45 | 6.67 0.49       |
| IRAS 09022-3615 | 7.46 1.8 | 5.65 0.30 | 7.26 0.74       |
| Arp 220    | 18.9 5.8       | 19.5 1.6       | 23.6 5.1        |
| Mrk 273   | 5.05 0.97      | 5.03 0.22      | 7.88 0.58       |
| UGC 05101 | ... ...        | ... ...        | 12.3 0.89       |
| NGC 6240  | 16.7 1.4       | 34.9 1.3       | 33.2 0.86       |
| Arp 299-C | 10.6 2.0       | 14.3 0.41      | 30.7 1.2        |
| Arp 299-B | 10.6 2.0       | 13.5 0.38      | 28.6 1.2        |
| Arp 299-A | 13.4 2.5       | 23.9 0.54      | 36.2 2.0        |
| NGC 1068  | 81.1 5.0       | 101 1.4        | 358 7.7         |
| NGC 1365-SW | 39.9 2.3   | 43.1 0.70      | 192 1.4         |
| NGC 1365-NE | 47.2 3.0  | 48.4 0.68      | 156 1.3         |
| NGC 4038  | 5.44 1.8       | 9.02 0.81      | 27.6 0.96       |
| NGC 4038 (Overlap) | 15.8 1.3 | 14.9 0.51      | 27.5 1.8        |
| M82       | 175 16         | 315 3.7        | 867 6.2         |
| IRG 1222  | ... ...        | 2.96 0.30      | 8.34 0.30       |
| M83       | 27.7 2.7       | 51.9 1.2       | 219 2.2         |
| NGC 253   | 262 21         | 387 5.8        | 357 18          |
| NGC 1266  | 7.97 1.4       | 11.4 0.31      | 7.51 1.0        |
| Cen A     | 39.4 2.1       | 93.8 0.57      | 102 1.0         |

Note. See Table 3 for more information.

(NGC 4038, NGC 1365, Arp 299) because fluxes separated into individual components were often not available. We used the dust model as in Casey (2012), which is the sum of a graybody and a power law with exponential drop-off:

\[
S(\lambda) = N_{bb} \frac{(1 - e^{-\lambda_0/\lambda})^3(c/\lambda)^{\beta}}{\lambda_0^{\beta}} + N_{pl} \lambda^\alpha e^{-(\lambda/\lambda_c)^2}. \tag{1}
\]

In Equation (1), the free parameters are \( T \) (temperature, K), \( \beta \) (emissivity index), \( \lambda_0 \) (wavelength at which optical depth is unity, \( \mu \)m), and \( \alpha \) (slope of the mid-IR power law). \( N_{bb} \), the normalization in Jy for the graybody component, is fixed at the best-fit value for any given combination of the previous parameters. \( \lambda_c \) and \( N_{pl} \) are tied to the other parameters as in Casey (2012, Table 1). In calculating the likelihood of the dust parameters, we assume that calibration errors are 50% correlated between measurements from the same instruments. We expect some degree of correlation, but too far above 50% in the covariance matrix can drive the best fit very far away from the data points of other instruments.
The results are shown in Figures 6 (best-fit spectral energy distribution; SEDs) and 7 (histogram of best-fit parameters). The individual parameter results are in Table 14. In all cases, only one mode in likelihood space was found, and the resulting likelihood distributions were very well defined by Gaussians (the best-fit and the mode and median of the resulting marginalized parameters all aligned).

Table 15 also lists the results for parameters that can be derived from the model above: the optical depth at 100 μm (τ_{100}), the dust mass (M_{dust}), and the far-infrared luminosity from 8 to 1000 μm (L_{8-1000} μm or L_{FIR}). To calculate the dust mass, we utilize $\kappa_{125,μm} = 2.64 m^2/kg^{-1}$ (Dunne et al. 2003) and $M_d = \frac{S_ν D_t^2 \kappa_ν B_ν(T)}{c}$ (statistical errors in Table 15 do not include uncertainty in $\kappa$). The values of $L_{FIR}$ we find when modeling the SED ($L = 4\pi D_t^2 \int_8^{1000} S_ν dν$) are slightly higher than those derived from utilizing only the 60 and 100 μm fluxes (e.g., those presented in Table 1 from Hyperleda), by about a factor of 1.7 ± 0.5.

Casey (2012) modeled 65 local LIRGS and ULIRGS, fixing $λ_0 = 200 μm$ and finding a mean $β = 1.60 ± 0.38$ and $α = 2.0 ± 0.5$. We find, in Figure 7 that $β$ and $α$ can vary significantly, but cluster around similar values. When left to vary, $λ_0$ can often be higher than 200 μm.
### Table 7
Photometry Flux Densities: IRAS

| Galaxy            | 12 μm  | 25 μm  | 60 μm  | 100 μm | Ref |
|-------------------|--------|--------|--------|--------|-----|
| Mrk 231           | 1.83   | 0.184  | 8.84   | 0.884  | 30.8 | 3.08 | 29.7 | 2.98 | 1 |
| IRAS F17207-0014  | 0.200  | 0.0320 | 1.61   | 0.164  | 32.1 | 3.21 | 36.1 | 3.65 | 1 |
| IRAS 09022-3615   | 0.200  | 0.0377 | 1.19   | 0.121  | 11.6 | 1.17 | 11.1 | 1.16 | 1 |
| Arp 220           | 0.610  | 0.0645 | 8.00   | 0.801  | 104  | 10.4 | 115  | 11.5 | 1 |
| Mrk 273           | 0.240  | 0.0294 | 2.36   | 0.237  | 22.5 | 2.25 | 22.5 | 2.25 | 1 |
| UGC 05101         | 0.250  | 0.0368 | 1.02   | 0.106  | 11.7 | 1.17 | 19.9 | 2.00 | 1 |
| NGC 6240          | 0.590  | 0.0641 | 3.55   | 0.356  | 22.9 | 2.29 | 26.5 | 2.65 | 1 |
| Arp 299-A         | 3.97   | 0.0398 | 24.5   | 2.45   | 113  | 11.3 | 111  | 11.1 | 1 |
| NGC 1365-NE       | 5.12   | 0.0413 | 14.3   | 1.43   | 94.3 | 9.43 | 166  | 16.6 | 1 |
| NGC 4038 (Overlap)| 1.94   | 0.0199 | 6.54   | 0.655  | 45.2 | 4.52 | 87.1 | 8.71 | 1 |
| M82               | 79.4   | 7.94   | 333    | 33.3   | 1480 | 148  | 1370 | 137  | 1 |
| NGC 1222          | 0.500  | 0.0550 | 2.28   | 0.231  | 13.1 | 1.31 | 15.4 | 1.54 | 1 |
| M83               | 21.5   | 2.15   | 43.6   | 4.36   | 266  | 26.6 | 524  | 52.4 | 1 |
| NGC 253           | 41.0   | 4.10   | 155    | 15.5   | 968  | 96.8 | 1290 | 129  | 1 |
| NGC 1266          | 0.250  | 0.0391 | 1.20   | 0.124  | 13.1 | 1.31 | 16.9 | 1.70 | 1 |
| Cen A             | 22.2   | 2.22   | 28.3   | 2.83   | 213  | 21.3 | 412  | 41.2 | 1 |

Reference (1) Sanders et al. 2003.

### Table 8
Photometry Flux Densities: MIPS

| Galaxy            | 24 μm  | 70 μm  | 160 μm | Ref |
|-------------------|--------|--------|--------|-----|
| Mrk 231           | 4.34   | ...    | ...    | 1   |
| Arp 220           | 4.01   | 0.449  | 80.8   | 14.6 | 1 |
| Mrk 273           | 1.86   | 0.208  | 20.2   | 3.64 | 11.7 | 3.69 | 1 |
| UGC 05101         | 0.808  | 0.0902 | 13.2   | 2.38 | 13.4 | 4.24 | 1 |
| Arp 299-A         | 8.66   | 0.0500 | ...    | ...  | ...  | ...  | ...  | 2 |
| NGC 1068          | 80.0   | 8.00   | 180    | 18.0 | ...  | ...  | ...  | 3 |
| NGC 4038 (Overlap)| 6.13   | 0.0450 | ...    | ...  | ...  | ...  | ...  | 2 |
| M83               | 42.0   | 4.20   | ...    | ...  | ...  | ...  | ...  | 3 |
| NGC 253           | 140.   | 14.0   | ...    | ...  | ...  | ...  | ...  | 3 |
| NGC 1266          | 0.880  | 0.0533 | 12.7   | 1.38 | 10.3 | 1.76 | 4, 5 |

References (1) U et al. 2012; (2) Lanz et al. 2013; (3) NED; (4) Dale et al. 2007; (5) Temi et al. 2009.

### Table 9
Photometry Flux Densities: PACS

| Galaxy            | 75 μm  | 110 μm | 170 μm | Ref |
|-------------------|--------|--------|--------|-----|
| Arp 299-A         | 139    | 13.9   | 127    | 12.7 | 74.2 | 7.42 | 1 |
| NGC 4038 (Overlap)| 81.0   | 8.11   | 116    | 11.6 | 99.8 | 9.98 | 1 |
| M82               | 1990   | 198    | ...    | ...  | 1290 | 129  | 1 |

Reference (1) Lanz et al. 2013.

### 3.2. CO Modeling Likelihood with Multinest

#### 3.2.1. Measurements from the Literature and Dust Optical Depth Correction

As discussed in Section 1, previous work has shown that the high-J lines detected by the FTS are often emitted by a warmer component of gas than the low-J lines. To accurately model both components of gas, we supplemented our FTS line fluxes with measurements from the ground of $J = 1 \rightarrow 0$, $J = 2 \rightarrow 1$, and $J = 3 \rightarrow 2$. The measurements used for this survey are presented in Table 16. We first utilized large surveys for consistent data; some galaxies had multiple measurements for the same line because of overlaps of the surveys. When surveys alone did not have enough lines for a particular galaxy, we sought out individual measurements in the literature. For the cases of semi-extended sources that may have multiple pointings, see Appendix A for more information on how these were handled. No ground-based measurements for IRAS 09022-3615 were available, so only the warm, high-J component of gas was modeled for this galaxy.
For comparison, at mid- to far-infrared wavelengths, the shape of the SLED in this fashion. To be explicit, the likelihood distributions, other than slight increases in the warm components, were found to be approximately linearly from 0.90 in the mean. The correction factor at CO 1−0 was 3.47 ± 0.026. We divided all flux densities by this factor for a mixed model, where we model the warm dust. At higher frequencies, the optical depth is not negligible. Discrepancy from the rest of the SLED.

We corrected the lines by dividing by this factor for a mixed model, where we model the warm dust. At higher frequencies, the optical depth is not negligible. Discrepancy from the rest of the SLED.

We additionally corrected the line fluxes for obscuration by dust. At higher frequencies, the optical depth is not negligible. We corrected the lines by dividing by this factor for a mixed model, where we model the warm dust. At higher frequencies, the optical depth is not negligible. Discrepancy from the rest of the SLED.

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The low-J line measurements came from a variety of telescopes with different beam sizes. We divided all flux densities in Jy km s⁻¹ by the appropriate η(Ω₈₅₀, Ω₄₃₅) from Table 2 to refer all fluxes to our beam size of 43′′ (see Section 2.2). The specific value used for each line flux in the last column of Table 16. In some cases, we gathered multiple transitions of the same line, and only discarded measurements that were wildly discrepant from the rest of the SLED.

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We additionally corrected the line fluxes for obscuration by dust. At higher frequencies, the optical depth is not negligible. We corrected the lines by dividing by this factor for a mixed model, where we model the warm dust. At higher frequencies, the optical depth is not negligible. Discrepancy from the rest of the SLED.
### Table 12
Photometry Flux Densities: ISO

| λ (μm) | $F_\nu$ (Jy) | $\sigma_{\text{tot}}$ (Jy) | Ref | λ (μm) | $F_\nu$ (Jy) | $\sigma_{\text{tot}}$ (Jy) | Ref | λ (μm) | $F_\nu$ (Jy) | $\sigma_{\text{tot}}$ (Jy) | Ref |
|--------|--------------|----------------------------|-----|--------|--------------|----------------------------|-----|--------|--------------|----------------------------|-----|
| Mrk 231 | 52 | 121 | 10.8 | 2 | 120 | 25.9 | 7.88 | 1 |
| 10 | 1.43 | 0.478 | 1 | 57 | 134 | 11.8 | 2 | 122 | 20.8 | 3.70 | 2 |
| 12 | 2.40 | 0.805 | 1 | 60 | 113 | 38.0 | 1 | 145 | 17.9 | 3.10 | 2 |
| 15 | 2.90 | 0.973 | 1 | 63 | 148 | 15.0 | 2 | 150 | 18.9 | 5.75 | 1 |
| 25 | 8.66 | 2.90 | 1 | 88 | 151 | 18.7 | 2 | 158 | 16.8 | 2.80 | 2 |
| 52 | 32.4 | 3.20 | 2 | 90 | 112 | 37.4 | 1 | 170 | 11.5 | 2.10 | 2 |
| 57 | 37.2 | 3.60 | 2 | 120 | 109 | 33.2 | 1 | 170 | 16.7 | 1.67 | 3 |
| 60 | 31.7 | 10.6 | 1 | 122 | 118 | 9.50 | 2 | 180 | 12.7 | 3.87 | 1 |
| 63 | 42.9 | 4.00 | 2 | 145 | 100 | 19.9 | 2 | 150 | 16.7 | 2.80 | 2 |
| 88 | 52 | 129 | 12.3 | 2 | 90 | 112 | 37.4 | 1 | 158 | 84.5 | 8.50 | 2 |
| 120 | 24.3 | 7.40 | 1 | 122 | 118 | 9.50 | 2 | 180 | 12.7 | 3.87 | 1 |
| 122 | 19.5 | 1.70 | 2 | 170 | 77.1 | 6.70 | 2 | 180 | 64.0 | 19.4 | 1 |
| 145 | 16.0 | 1.70 | 2 | 170 | 77.1 | 7.71 | 3 | 63 | 151 | 14.6 | 2 |
| 150 | 14.7 | 4.80 | 2 | 180 | 110 | 14.6 | 2 | 170 | 8.30 | 2.10 | 3 |
| 158 | 16.1 | 2.20 | 2 | Mrk 273 | 145 | 65.7 | 5.30 | 2 |
| 170 | 15.3 | 1.60 | 2 | 158 | 58.6 | 7.50 | 2 |
| 170 | 15.3 | 1.53 | 3 | 150 | 14.7 | 4.80 | 2 | 180 | 6.88 | 2.09 | 1 |
| 180 | 9.75 | 2.97 | 1 | 15 | 4.44 | 0.444 | 3 |
| 200 | 6.88 | 2.09 | 1 | 145 | 65.7 | 5.30 | 2 |
| 10 | 0.080 | 0.027 | 1 | 15 | 4.44 | 0.444 | 3 |
| 12 | 0.200 | 0.067 | 1 | 12 | 0.750 | 0.252 | 1 | NGC 1266 |
| 15 | 0.250 | 0.084 | 1 | 15 | 1.00 | 0.335 | 1 |
| 25 | 1.32 | 0.443 | 1 | 170 | 26.4 | 2.64 | 3 |
| 52 | 40.7 | 4.90 | 2 | 180 | 10.1 | 1.01 | 3 |
| 57 | 31.6 | 2.70 | 2 | 180 | 10.1 | 1.01 | 3 |
| 60 | 32.2 | 10.8 | 1 | 122 | 12.9 | 1.10 | 2 |
| 63 | 41.9 | 3.90 | 2 | 158 | 14.8 | 4.80 | 2 |
| 88 | 48.5 | 4.90 | 2 | 150 | 13.1 | 3.98 | 1 |
| 90 | 31.9 | 10.7 | 1 | 158 | 10.8 | 2.20 | 2 |
| 120 | 30.0 | 9.12 | 1 | 122 | 12.9 | 1.10 | 2 |
| 145 | 27.0 | 2.50 | 2 | 180 | 6.88 | 2.09 | 1 |
| 150 | 25.0 | 7.00 | 1 | 150 | 26.4 | 2.64 | 3 |
| 158 | 23.0 | 2.00 | 1 | 150 | 26.4 | 2.64 | 3 |
| 170 | 24.3 | 2.90 | 2 | Mrk 273 | 145 | 65.7 | 5.30 | 2 |
| 170 | 26.4 | 3.20 | 2 | 145 | 65.7 | 5.30 | 2 |
| 170 | 26.4 | 2.97 | 1 | 156 | 23.0 | 7.00 | 1 |
| 180 | 17.5 | 5.32 | 1 | 170 | 8.30 | 0.830 | 3 |
| 200 | 12.5 | 3.80 | 1 | 170 | 8.30 | 0.830 | 3 |
| 25 | 8.28 | 2.78 | 1 | 170 | 8.30 | 0.830 | 3 |
| References. (1) Klaas et al. 2001; (2) Brauher et al. 2008; (3) NED. |

### Table 13
Photometry Flux Densities: All Others

| λ (μm) | $F_\nu$ (Jy) | $\sigma_{\text{tot}}$ (Jy) | Ref |
|--------|--------------|----------------------------|-----|
| Mrk 231 | 880 | 0.056 | 0.006 | 1 |
| 350 | 1.73 | 0.173 | 1 |
| 880 | 0.080 | 0.008 | 1 |
| Arp 220 | 250 | 363 | 25.4 | 2 |
| 350 | 9.74 | 0.974 | 1 |
| 880 | 0.490 | 0.049 | 1 |
| Mrk 273 | 500 | 49.6 | 4.80 | 2 |
| 350 | 1.77 | 0.177 | 1 |

References. (1) NED; (2) Lanz et al. 2013.

$\Omega_b = 5.04 \times 10^{-8}$ sr corresponds to areas of $5.04 \times 10^4(D_L(1 + z)^{-2})^2$ pc$^2$. Note that both $A$ and $\Phi_A$, the area filling factor, are present in this equation, which accounts for beam dilution for the many sources that are less than 43.5′′ across. The factor of 1.4 accounts for helium and other heavy elements, and $X_{12\text{CO}}$ is the abundance ratio of 12CO to H$_2$: we use $2 \times 10^{-4}$. We also calculated the probabilities of the total CO luminosity in each component from RADEX, which may include contributions from higher-$J$ lines other than those modeled here. Finally, we also determined the likelihood for the ratio of warm to cold properties (e.g., $M_1/M_2$). The temperature and density are degenerate; even when one might not individually be well determined, their product (thermal pressure, henceforth simply “pressure”) is better constrained because the two properties are anti-correlated.
Likewise, the column density and filling factor are degenerate, and it is their product (proportional to mass) that is better determined. However, it is important to note that these two parameters are not perfectly degenerate. Pressure is largely responsible for the shape of the SLED, and mass for the absolute flux scaling. The filling factor linearly scales the absolute values (i.e., the normalization) of the peak temperatures in the CO SLED, while varying the column density changes the absolute values as well as the SLED shape, as a result of optical depth effects. Thus the model SLEDs depend on both quantities independently, and so column density and filling factor are separate parameters. We adopted $\Omega_s = 1.133 \times 43.5^2$ sq arcsec, allowing $\Phi_A$ to account for emission smaller than the extent of the beam.

### 3.2.3. Model Constraints and Priors

RADEX calculates antenna temperatures in K, so we converted our data from Jy km s$^{-1}$ to K km s$^{-1}$ by multiplying...
by 646 $\nu^2$ (assuming the aforementioned 43′′ beam). We then divided our integrated flux data into per-unit-linewidth units of temperature (K instead of K km s$^{-1}$) to directly compare to RADEX, assuming fixed linewidths. This is because the actual parameter we were testing was column density per unit linewidth; the modeled emission was simply multiplied by linewidth. Because the FTS did not resolve the widths of the lines, we relied on ground-based CO measurements for linewidths. The values used are in Table 17; many are medians of multiple CO linewidths from the literature, if more than one measurement was available. Our reported masses and luminosities scale linearly with linewidth.

Given the size of the eight-dimensional parameter space, it was important to apply some physical constraints to limit the potential solutions to those that are physically meaningful. Some of these constraints were on the relationship between the two components: we required the first component to be cooler

Table 14

Dust Fitting Results: Model Parameters

| FTS Name          | $\lambda_0$ (μm) | $\beta$ | $T$ (K) | $\alpha$ |
|-------------------|------------------|---------|---------|----------|
|                   | Mean $\sigma$    | Best    | Mean $\sigma$ | Best    | Mean $\sigma$ | Best |
| Mrk 231           | 231              | 24      | 242     | 1.82     | 0.12       | 1.85  |
| IRAS F17207-0014  | 96               | 120     | 14.8    | 0.11     | 0.16       | 1.46  |
| IRAS 09022-3615   | 176              | 53      | 161     | 1.69     | 0.57       | 1.37  |
| Arp 220           | 187              | 193     | 1.54    | 0.09     | 0.15       | 1.54  |
| Mtk 273           | 115              | 25      | 136     | 1.58     | 0.07       | 1.60  |
| UGC 05101         | 225              | 50      | 225     | 1.94     | 0.42       | 1.87  |
| NGC 6240          | 226              | 46      | 212     | 1.65     | 0.25       | 1.60  |
| Arp 299-A         | 120              | 30      | 140     | 1.26     | 0.08       | 1.28  |
| NGC 1068          | 244              | 34      | 251     | 1.80     | 0.09       | 1.82  |
| NGC 1365-NE       | 181              | 64      | 61      | 1.45     | 0.08       | 1.39  |
| NGC 4038 (Overlap)| 219              | 31      | 220     | 1.87     | 0.11       | 1.88  |
| M82               | 137              | 44      | 100     | 1.30     | 0.06       | 1.30  |
| NGC 1222          | 205              | 49      | 226     | 1.48     | 0.17       | 1.49  |
| M83               | 213              | 49      | 211     | 1.59     | 0.09       | 1.60  |
| NGC 253           | 267              | 28      | 294     | 1.46     | 0.07       | 1.50  |
| NGC 1266          | 206              | 25      | 214     | 2.00     | 0.29       | 2.04  |
| Cen A             | 187              | 66      | 64      | 0.71     | 0.10       | 0.68  |

Note. The statistical error on $M_{\text{dust}}$ does not include the uncertainty in the dust emissivity.

Table 15

Dust Fitting Results: Derived Parameters

| FTS Name          | $\tau_{100}$ | $\log M_{\text{dust}} \left[ M_\odot \right]$ | $\log L_{8-1000\mu m} \left[ L_\odot \right]$ |
|-------------------|--------------|---------------------------------|----------------------------------|
|                   | Mean $\sigma$ | Best                            | Mean $\sigma$ | Best | Mean $\sigma$ | Best |
| Mrk 231           | 5.18         | 1.46                            | 5.57   | 7.80 | 0.02       | 7.80  |
| IRAS F17207-0014  | 1.04         | 0.42                            | 1.39   | 8.32 | 0.05       | 8.28  |
| IRAS 09022-3615   | 4.08         | 3.61                            | 2.09   | 7.96 | 0.07       | 7.90  |
| Arp 220           | 2.80         | 0.79                            | 2.85   | 8.08 | 0.02       | 8.07  |
| Mtk 273           | 1.36         | 0.47                            | 1.75   | 7.77 | 0.06       | 7.71  |
| UGC 05101         | 6.78         | 4.58                            | 4.91   | 8.27 | 0.07       | 8.27  |
| NGC 6240          | 4.55         | 2.34                            | 3.49   | 7.69 | 0.06       | 7.71  |
| Arp 299-A         | 1.31         | 0.45                            | 1.56   | 7.46 | 0.03       | 7.44  |
| NGC 1068          | 5.22         | 1.46                            | 5.41   | 7.49 | 0.07       | 7.48  |
| NGC 1365-NE       | 2.56         | 1.34                            | 0.51   | 7.56 | 0.09       | 7.72  |
| NGC 4038 (Overlap)| 4.59         | 1.45                            | 4.47   | 7.43 | 0.06       | 7.43  |
| M82               | 1.56         | 0.68                            | 1.00   | 6.45 | 0.09       | 6.53  |
| NGC 1222          | 3.18         | 1.38                            | 3.45   | 6.31 | 0.06       | 6.27  |
| M83               | 3.52         | 1.35                            | 3.51   | 7.07 | 0.07       | 7.08  |
| NGC 253           | 4.28         | 0.77                            | 5.05   | 6.78 | 0.06       | 6.77  |
| NGC 1266          | 4.69         | 1.94                            | 4.82   | 6.34 | 0.04       | 6.33  |
| Cen A             | 1.57         | 0.46                            | 0.75   | 6.51 | 0.05       | 6.56  |

Note. The statistical error on $M_{\text{dust}}$ does not include the uncertainty in the dust emissivity.
Table 17. The length upper limits were calculated by fitting

| Jup  | Δν  | σ  | η(Ω) | Ref     | Jup  | Δν  | σ  | η(Ω) | Ref     |
|------|-----|----|------|---------|------|-----|----|------|---------|
| 1    | 73.5| 15 | 1.00 | 1       | 1    | 403 | 22 | 1.00 | 7       |
| 2    | 70.3| 18 | 1.00 | 2       | 1    | 609 | 120| 0.90 | 1       |
| 3    | 73.6| 15 | 1.00 | 3       | 1    | 283 | 56 | 1.04 | 14      |
| 4    | 350.| 81 | 1.00 | 2       | 1    | 520 | 57 | 1.04 | 15      |
| 5    | 609.| 130| 1.00 | 2       | 1    | 1780| 350| 0.89 | 16      |
| 6    | 561.| 630| 0.49 | 5       | 1    | 2210| 35 | 1.00 | 19      |
| 7    | 468.| 93 | 0.98 | 4       | 1    | 2160| 440| 1.01 | 3       |
| 8    | 651.| 72 | 1.04 | 7       | 1    | 6670| 1300| 0.75| 18      |
| 9    | 2230| 230| 0.65 | 5       | 1    | 12100|1100| 0.52| 20      |
| 10   | 2830| 410| 0.98 | 4       | 1    | 1500| 300 | 1.18 | 17      |
| 11   | 4600| 1300|0.46| 6       | 1    | 1860| 370 | 1.01 | 18      |
| 12   | 3870| 410 |0.46| 5       | 1    | 2140| 430 | 1.02 | 3       |
| 13   | 5720| 5500|0.62| 8       | 1    | 5550| 1100| 0.58 | 18      |
| 14   | 68200|7800|0.19| 5       | 1    | 82.3 | 15 | 1.00 | 2       |
| 15   | 6600| 650 |1.02 | 7       | 1    | 90.0 | 18 | 1.00 | 1       |
| 16   | 37400|3600|0.62| 8       | 1    | 68.1 | 14 | 1.00 | 14      |
| 17   | 52000|5500|0.62| 8       | 1    | 82.3 | 15 | 1.00 | 2       |
| 18   | 68200|7800|0.19| 5       | 1    | 112 | 28 | 1.00 | 21      |
| 19   | 2230| 330 |1.03 | 7       | 1    | 97.6 | 19 | 1.00 | 3       |
| 20   | 4240| 840 |0.45 | 3       | 1    | 273 | 54 | 1.00 | 2       |
| 21   | 11700|1100|0.74| 9       | 1    | 491 | 110 | 1.00 | 2       |
| 22   | 12600|2500|0.16| 3       | 1    | 10800|1100| 1.01 | 7       |
| 23   | 17800|3000|1.00| 10      | 1    | 90.4 | 13 | 1.00 | 7       |
| 24   | 11800|3400|0.48| 8       | 1    | 103 | 20 | 1.00 | 1       |
| 25   | 1540| 290 |1.01| 11      | 1    | 88.5 | 16 | 1.00 | 2       |
| 26   | 1620| 170 |1.04| 12      | 1    | 83.7 | 12 | 1.00 | 15      |
| 27   | 3440| 430 |0.48| 12      | 1    | 104 | 21 | 1.00 | 3       |
| 28   | 2020| 200 |1.02| 7       | 1    | 327 | 56 | 1.00 | 2       |
| 29   | 3660| 370 |0.76| 5       | 1    | 592 | 120 | 1.00 | 2       |
| 30   | 10500|2300|0.54| 13      | 1    | 354 | 110 | 1.00 | 6       |
| 31   | 13400|3800|0.57| 6       | 1    | 376 | 46 | 1.00 | 5       |
| 32   | 8680| 830 |0.57| 5       | 1    | 12100|350| 1.00 | 2       |

Note. Calibration errors, from references or assumed, are included in σ.

References. (1) Solomon et al. 1997; (2) Papadopoulos et al. 2012; (3) Baan et al. 2008; (4) Schirm et al. 2014; (5) Bayet et al. 2006; (6) Mao et al. 2010; (7) Young et al. 1995; (8) Ward et al. 2003; (9) Kamenetzky et al. 2011; (10) Spinoglio et al. 2012; (11) Wild & Eckart 2000; (12) Eckart et al. 1996; (13) Mauersberger et al. 1999; (14) Sanders et al. 1991; (15) Maiolino et al. 1997; (16) Greve et al. 2009; (17) Papadopoulos & Seaquist 1998; (18) Sandqvist et al. 1995; (19) Elfhag et al. 1996; (20) Sandqvist et al. 1999; (21) Albrecht et al. 2007; (22) Sliwa et al. 2012; (23) Harrison et al. 1999; (24) Z-Spec; (25) Alatalo et al. 2011; (26) Young et al. 2011.

than the second (henceforth referred to as the “cool/cold” and “warm” components), and the cool component to contain more mass than the warm.

Two additional priors were used based on known physical constraints: the sum of the two components’ mass could not exceed the dynamical mass of the galaxy, nor could either component’s line-of-sight length be greater than the extent of the galaxy in the plane of the sky. The mass as a function of our parameters is that given in Equation (2); the dynamic mass sets the galaxy in the plane of the sky. The mass as a function of our parameters is N_{CO}(\sqrt{\Phi_1}H_2X_{CO})^{-1}. The dynamical mass and length limits are presented in Table 17. The length upper limits were calculated by fitting a two dimensional Gaussian to the SPIRE PSW maps. This Gaussian was the convolution of the intrinsic source size and the PSW beam (FWHM = 19.3'). We used the longest length of the Gaussian (g) and found the source size, \sigma = \sqrt{\sigma^2-19.3'^2}. We utilized the largest-size-of-a-Gaussian approximation because we sought only an upper limit. The dynamical mass limit was determined from the linewidth (ΔV) and maximum length limit L, such that M_{max} = ΔV^2L/G. If any of these constraints were violated, the likelihood for that set of parameters was not included.

Furthermore, any one line was not counted in the likelihood if its modeled optical depth was less than −0.9 or greater than 100. The upper limit of 100 was because the concept of a
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The extinction correction affected the high-J CO lines the most, increasing their fluxes more than low-J lines and thus affecting the shapes of the SLEDs. When we use non-extinction corrected fluxes in modeling, we found that the distribution of parameters were not statistically significantly different given the errors bars. The most noticeable difference was the warm pressure, which was only 0.1 dex higher when dust correction is included (this is expected because overall shape of the SLED is determined by the pressure). The CO luminosity generally peaks at mid-J lines not as strongly affected by extinction (e.g., $J = 6 \rightarrow 5$).

Of the maximum mass and length priors, the length turned out to limit only a very small section of the allowed parameter space. The dynamical mass was the more restrictive prior. When modeled without the maximum mass and length priors, the marginalized parameter likelihoods for most of our galaxies were indistinguishable from modeling with the priors. This means the priors did not have a significant effect (i.e., the combinations of parameters violating these priors did not contribute significantly to the likelihood anyway due to poor match to the data). Only a few showed an appreciable difference (M82, Arp 220, and NGC 253), generally by allowing an unconstrained high-mass shoulder, but not changing the location of the main likelihood peak.

3.3. LTE Analysis of [C 1]

Two forbidden lines of neutral carbon ([C 1]) were present in our spectra. The ratios of the line intensities in Jy km s$^{-1}$ ($J = 2 \rightarrow 1/1J = 1 \rightarrow 0$) were used to derive excitation temperatures, equivalent to the kinetic temperatures of the [C 1] emitting gas under the assumption of local thermodynamic equilibrium:

$$T_{\text{ex}} = E_{21} \left[ \ln \left( \frac{g_2 A_{21} S_{10}}{g_1 A_{10} S_{21}} \right) \right]^{-1}.$$  (3)

In the above equation, $A$ is the statistical weight of a level, $E_{21}$ the difference in energy levels in K (as we will use through the remainder of the section), and $S$ the flux in Jy km s$^{-1}$. (If using the ratio in K km s$^{-1}$ or W m$^{-2}$, one must also include $\lambda_{10}/\lambda_{21}$ in the natural log term above.)

We corrected each flux to account for the absorption by dust as described in Section 3.2.1. Each integrated flux in LTE is proportional to the population level of the upper state of the line, where $N_j$ equals $L_{J \rightarrow J}/(A_{J \rightarrow J} h \nu_{J \rightarrow J})$. The total number of atoms or molecules can be found by dividing by the fraction of those in that state, where $f_i = g_i e^{-E_i/T_{\text{ex}}}/Z(T_{\text{ex}})$ and $Z(T_{\text{ex}})$ is the partition function, $Z(T_{\text{ex}}) = \sum_i g_i e^{-E_i/T_{\text{ex}}}$. The total mass is therefore $mN_j/f_i$, where $m$ is the mass of the atom or molecule. Temperatures and masses (calculated from the $J = 2$ energy level, as these lines have the lowest error in flux) are in Table 21. We further discuss these results in Section 4.5.

3.4. LTE Analysis of H$_2$

CO is used as a proxy for total molecular gas, most of which is molecular hydrogen. The electric quadrupole transitions of H$_2$ are difficult to observe, but were available for many of these bright galaxies. Here we consider the S(0), S(1), S(2), S(3), S(5), and S(7) transitions of H$_2$. The hydrogen fluxes and optical depths are in Table 22; see Appendix A for detailed information.

| FTS Name | Linewidth (km s$^{-1}$) | Length Max (pc) | Mass Max (10$^5$ $M_\odot$) |
|----------|------------------------|----------------|-----------------------------|
| Mkr 231  | 198                    | 1415           | 65                          |
| IRAS F17207-0014 | 373                    | 5384           | 869                         |
| IRAS 09022-3615 | 547                    | 5650           | 1961                        |
| Arp 220  | 428                    | 4739           | 1008                        |
| Mkr 273  | 265                    | 5090           | 417                         |
| UGC 05101 | 350                    | 3955           | 562                         |
| NGC 6240 | 390                    | 8770           | 1399                        |
| Arp 299-C | 80                     | 6351           | 47                          |
| Arp 299-B | 155                    | 6353           | 177                         |
| Arp 299-A | 282                    | 6349           | 586                         |
| NGC 1068 | 254                    | 3454           | 258                         |
| NGC 1365-SW | 250                  | 2567           | 136                         |
| NGC 1365-NE | 250                  | 2564           | 135                         |
| NGC 4038 | 133                    | 4900           | 101                         |
| NGC 4038 (Overlap) | 166                | 5922           | 189                         |
| M82      | 174                    | 850            | 30                          |
| NGC 1222 | 80                     | 2703           | 20                          |
| M83      | 102                    | 1169           | 14                          |
| NGC 253  | 220                    | 402            | 23                          |
| NGC 1266 | 239                    | 576            | 38                          |
| Cen A    | 150                    | 1998           | 52                          |

Notes. See Section 3.2.3. The CO likelihood also depends on the luminosity distance, given in Table 1, and the beam area. All are normalized to $\Omega_k = 5.04 \times 10^{-8}$ sr, see Section 2.2. Linewidths are the average of those reported from references in Table 16. No linewidths were available for NGC 1365-NE, NGC 1365-SW, NGC 1222, and IRAS 09022-3615; the $v_{rot}$ from Hyperleda was used instead for the first three, and the [O III] linewidth was used for the last from Lee et al. (2011).

One-zone model breaks down at this point. The line center optical depths are so large that the measured excitation temperatures will vary strongly across the line profile, causing self-absorption. In other words, the escape probability method becomes invalid. We allowed a slightly negative lower limit because we found that, even given normal ISM conditions, the lowest population levels may be slightly inverted (resulting in negative optical depth). Again, the escape probability method can no longer be used with a strong maser.

The results are presented in Figures 8, 9, 10, 11, 12, and 13, and Tables 18, 19, and 20. As with the dust modeling results in the previous section, we present the mode mean, mode sigma, and best-fit results (recall Section 3 for these terms). However, the likelihood distributions themselves (in the accompanying figures) are not as simply described as in the dust modeling case. In many instances, the best-fit result (and the associated SLED illustrated in 8) does not correspond to the mean or mode of a marginalized parameter distribution. Additionally, the results for some galaxies included contributions from multiple modes, which can be thought of as separate islands in parameter space. The mode mean and sigma presented here are for that of the mode containing the highest integrated likelihood; this mode had an obvious distinction as the far more likely mode than any other ones found.

3.2.4. Effects of Extinction Correction and Modeling Priors

In most cases, our use of extinction correction and mass and length priors did not significantly impact the results of the CO modeling, especially in the determination of the molecular mass, which will become important in the discussion of the results.
on extended galaxies. The derived temperatures and masses are in Table 23, with excitation diagrams in Figure 14. The ground state transition (at 510 K) is very insensitive to cold (tens of K) gas, so the hydrogen-derived masses in Table 23 necessarily miss much of the molecular mass.

With Equation (3), we calculated excitation temperatures for the following combination of lines (when available): \( S(1) \) and \( S(0) \); \( S(3) \), \( S(2) \), and \( S(1) \); \( S(7) \) and \( S(5) \). We also corrected these lines for dust extinction, but in this portion of the spectrum the notable feature is the 9.7 \( \mu \)m silicate absorption feature. Based on the extinction models of Draine (1989), we used \( \tau_{5}/\tau_{9.7} = 0.19, 0.35, 0.43, 0.99, 0.20, 0.30 \) for \( S(0) \), \( S(1) \), \( S(2) \), \( S(3) \), \( S(5) \), and \( S(7) \), and \( A_{V} = 1.086 \tau \). The values that we use for \( \tau_{9.7} \) are listed in the last column of Table 23.

In many cases, only an upper limit was available for \( S(0) \), meaning the \( S(1) - S(0) \) excitation temperature is a lower limit, and the \( S(0) \)-derived mass an upper limit.

One could calculate an excitation temperature from any pair of lines. The excitation temperature is the inverse of the slope of the lines presented in the excitation diagrams (Figure 14), which can be used to fit an excitation temperature to multiple lines, as we did with \( S(3) \), \( S(2) \), and \( S(1) \). One excitation temperature generally could not be fit for all lines from \( S(0) \) through \( S(7) \), which is why we present three. We did not calculate, for example, an excitation temperature from \( S(7) - S(3) \) when the \( S(5) \) line was unavailable, for consistency across the sample.

The extinction correction most dramatically increased the flux for the \( S(3) \) line because of its alignment in wavelength with the

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**Figure 8.** CO modeling spectral line energy distributions. The blue is the best-fit solution for the cold component and the red the best-fit solution for the warm, with their totals in gray. Those galaxies that contain all three of the lowest-\( J \) transitions also have a green line (dashed), which is the fit to only those three lines (see Section 4.1.3).

(A color version of this figure is available in the online journal.)
Figure 9. CO modeling likelihood results: pressure. Blue/red (diagonal/horizontal hatches) represent cool/warm components. Shaded areas indicate the 1σ uncertainty region, defined here as the mode median +/− the error (symmetric) on the parameter. Vertical lines represent the best-fit model parameter. IRAS F17207-0014 is an example of a galaxy with best-fit parameter values close to the median, whereas UGC 05101 is an example where the best-fit and median values do not align.

(A color version of this figure is available in the online journal.)

silicate absorption feature. Cen A is a good example of a galaxy with high extinction and many lines measured. The extinction correction raised the three temperatures by 6, 39, and 50 K. If we calculated separate excitation temperatures S(2)−S(1) and S(3)−S(2), with no extinction correction we found 392 ± 82 and 300 ± 39 K. With extinction correction, the temperatures were 406 ± 88 and 351 ± 54 K. The correction had the effect of increasing the two temperatures, but more importantly, bringing these three mid-excitation lines into better alignment, giving us a better estimate of one middle excitation temperature. (Notice that the S(2)−S(1) and S(3)−S(2) temperatures quoted above are not distinguishable within the error bars.)

For the conditions studied here, the first 5 H2 levels are likely in LTE, based on the collision rate coefficients in Le Bourlot et al. (1999). This assumption may become increasingly poor for the S(5) and S(7) lines, and the temperatures and masses from these lines should be treated as approximations.

3.5. [C II] and [N II] Line Ratios

Finally, we collected [C II] 158 μm fluxes for our sample of galaxies to compare to our FTS measured [N II] 205 μm line. The ratio of these two lines ([C II]/[N II]) from ionized gas is fairly constant, about 2.5 to 4.3, independent of ionized gas density (Oberst et al. 2006). This implies that ratios higher than this value indicate excess [C II] emission from other sources, especially photodissociation regions (PDRs). For example, a ratio of 30 indicates 8%−14% of [C II] emission from ionized gas, hence 92%−86% from other sources (for an assumed ionized ratio range of 2.5 to 4.3, respectively).
We present our results in Table 24, which includes the $[\text{C} \, \text{ii}]$ line fluxes used and the percentage of emission from ionized gas. In most of our galaxies, the majority of $[\text{C} \, \text{ii}]$ emission is from PDRs and other non-ionized sources, ranging from 48% to 96%. The median is 75%–85%. We discuss the meaning of this in Section 4.5.

4. DISCUSSION

This survey sought to answer a variety of questions related to the molecular ISM in galaxies, specifically those detailed in Section 1. The first subsection here addresses systematic effects of our modeling procedure, including aspects of two-component modeling that ought to be considered in future CO SLED modeling. The next two focus on two useful quantities derived from our data: the luminosity-to-mass conversion factor (Section 4.2) and gas-to-dust mass ratios (Section 4.3). Section 4.4 discusses trends in the molecular gas properties within our sample, and Section 4.5 specifically examines the difference in properties derived from C, C+, and CO. Finally, Section 4.6 compares the molecular gas properties to those of the Galactic Center and Sgr B2.

In the plots that follow, most parameters are plotted in log-log space, with bottom panels showing the ratio of the parameters. This is a small sample of diverse galaxies; the lines are meant to illustrate the presence or absence of general trends, but should be interpreted with caution. In some cases, our primary interest is whether two parameters have a linear relationship or not; to robustly determine the uncertainties, we used a case re-sampling nonparametric bootstrap method. For $n$ galaxies included in the fit, we drew $n$ samples (allowing re-selection of the same sample) and fit a line 1000 times; the error was then the 68% interval of the PDF of the resulting parameter fits.
Most previous studies of CO molecular gas properties were based on the few lines available in atmospheric windows. With three or four lines, only one component of cool molecular gas could be described with molecular excitation models such as RADEX, relying on four parameters. The first detections of CO \( J = 6 \rightarrow 5 \) by Harris et al. (1991) indicated higher-excitation gas than explained by CO \( J = 1 \rightarrow 0 \). Now with 10 additional lines available with Herschel, by visual inspection alone (Figure 5) one can see that additional excitation is required to explain high-\( J \) lines. This point has already become noticeable in the past few years (e.g., Panuzzo et al. 2010; Kamenetzky et al. 2012; Rangwala et al. 2011; Spinoglio et al. 2012; Rigopoulou et al. 2013; Hailey-Dunsheath et al. 2012; Pereira-Santaella et al. 2013) and was a major motivation for this study. For the past few years, FTS SLEDs have often been modeled using two or three distinct components, each described by its own set of physical parameters. This section will analyze the statistical validity and astrophysical meaning of such models.

### 4.1. Discussion of Systematic Effects of Simultaneous Two-component Modeling

We wish to emphasize that it is unlikely that all molecular gas is described either by our “cool” or “warm” component conditions. Rather, we recognize that it is likely that we are really measuring the sum of the emission from a wide distribution of molecular cloud properties. There may also be multiple components comprised of different ranges of conditions or distributions.
For example, the H$_2$ excitation ladders (Figure 14) clearly indicate a gradient in excitation temperatures (though we note that H$_2$ rotational lines are not sensitive to the coldest molecular gas). Higher lines of H$_2$ indicate higher temperatures and lower masses. In general, Table 23 shows that the mass in the few hundred K component ($T_{\text{u}}$) is 1%–20% of that in the colder gas traced by S(0). The S(5) and S(7) lines, which trace $>1000$ K gas, come from orders of magnitude smaller gas masses. In our two-component SLED modeling, we found typically 10% of the mass in very warm gas and 90% in cooler gas, but these two components are presumably sums over a range of gas conditions.

Increased effort has been made to describe the SLEDs that would result from, for example, a continuous distribution of temperatures. Neufeld (2012) created models with a power-law distribution in gas temperatures ($dN/dT \propto T^{-\beta}$, using a constant density) and found such models can describe CO rotational diagrams in the Herschel PACS range that cannot be described by an isothermal medium. Pereira-Santaella et al. (2014) applied the same concept to a sample of Seyferts observed by the FTS (including one from this work, UGC 05101); to fit both CO and H$_2$, they required a broken power law, and found that $\beta$ and $n_{\text{H}_2}$ were degenerate, for the same reasons we find $T$ and $n_{\text{H}_2}$ degenerate. Such models can influence the further discussion of excitation mechanisms, e.g., the extent to which PDRs or shocks may explain the CO emission.

However, a yet unresolved problem is the extent to which even high signal-to-noise ratio (S/N) CO SLEDs can distinguish a power-law distribution from distinct components. The resulting SLED from a power-law distribution can exactly imitate the emission from gas with a uniform temperature and different density, due to the degeneracy between $n_{\text{H}_2}$ and $T$. For example, Goicoechea et al. (2013) found the CO emission from Sgr A* can be described by either a single, hot, low-density component of gas or multiple, cooler components at higher density. The CO SLEDs alone do not provide the information necessary to distinguish the uniqueness of either type of model. Numerical simulations of galaxies, coupled with radiative transfer, could potentially deepen our understanding of how a gradient of excitation conditions adds up to produce the total emission we can measure (e.g., Narayanan & Krumholz 2014).

Therefore, differences in “cool” and “warm” component properties among galaxies can thus be indicating different underlying distributions of cloud physical conditions. In the rest of the discussion we continue to refer to these distinct components, but we caution the reader to interpret our conclusions with this important section in mind. The following subsections refer only to distinct component modeling, in order to compare with the majority of the Herschel FTS literature.

4.1.2. Adding Another Distinct Component

In the context of distinct components, we must address the question of why we modeled two components and not three or more. The simplest answer is that the SLEDs were statistically well described by eight parameters and hence there is no justification for adding a more complicated model where the number of free parameters approaches or exceeds the number of data points. One could cite “Occam’s Razor” and stop here. However, a more in-depth investigation is still informative, especially given our understanding of the more complicated physical situation we are attempting to describe. We emphasize that this subsection concerns our ability to detect the presence...
of three distinct components from the 13 lines of data we have; as already discussed, there is likely a continuous distribution of gas conditions, and we do not mean to imply that there are not actually three or more components physically present in the gas.

We sought to investigate if we could discern the temperature/mass components we see in H$_2$ (now referred to as Components I, II, and III) with the CO SLEDs. We used the same method as described in 3.2 (now requiring 12 free parameters) for two well-defined galaxy SLEDs (Arp 220 and M82). We applied some additional constraints: $T_I < T_{II} < T_{III}$, $M_I > M_{II} > M_{III}$, and we restricted the temperature ranges for each component, such that $0.5/2.3 < \log(T_I/T_{II}/T_{III}) < 2.3/3.5$. These ranges were meant to encompass the ranges seen in H$_2$, but we found qualitatively similar results without such restrictions (see Appendix A for Arp 220). The same priors as previously used were applied for optical depths, maximum length of any one component, and maximum total mass (Section 3.2.3).

The resultant best fits were nearly identical with the two-component fits (no improvement in total $\chi^2$), with Component I acting as the cool component and Component II as the warm. By this we mean that the pressure, luminosity, and mass distributions were significantly overlapping with our previous results (though discernible). We illustrate this in Appendix A for the case of Arp 220. Component III had negligible mass, negligible contribution to the total luminosity, and was poorly constrained otherwise. In other words, the CO SLEDs are not sensitive to the extremely low mass component derived from S(7)–S(5) hydrogen lines, absent additional strict prior constraints on the parameter space. Though one could exactly fix the mass and temperatures of each component to match that of hydrogen, we have no reason to believe that there is a
Table 19: CO Fitting Results: Derived Parameters

| FTS Name | log $L_{\text{CO}}$ (erg s$^{-1}$) Mean | log $L_{\text{CO}}$ (erg s$^{-1}$) σ | log $L_{\text{CO}}$ (erg s$^{-1}$) Best | log $P$ (K cm$^{-1}$) Mean | log $P$ (K cm$^{-1}$) σ | log $P$ (K cm$^{-1}$) Best | log $(N_{\text{CO}})$ (cm$^{-2}$) Mean | log $(N_{\text{CO}})$ (cm$^{-2}$) σ | log $(N_{\text{CO}})$ (cm$^{-2}$) Best | log $M_{\text{HI}}$ ($M_\odot$) Mean | log $M_{\text{HI}}$ ($M_\odot$) σ | log $M_{\text{HI}}$ ($M_\odot$) Best |
|----------|--------------------------------------|-----------------------------------|---------------------------------------|--------------------------|--------------------------|--------------------------|--------------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
| Cen A    | 38.7 0.3 38.5 4.1 0.9 3.7            |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Mrk 231  | 42.59 0.06 42.66 7.0 0.1 7.1         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| IRAS F17207-0014 | 42.37 0.03 42.37 7.3 0.3 7.1     |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Mrk 237  | 42.41 0.07 42.48 7.1 0.1 7.1         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| UGC 05101| 42.86 0.06 42.88 7.2 0.1 7.2         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 6240 | 42.41 0.08 41.36 5.3 0.3 5.4         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Arp 299-B| 41.49 0.04 41.36 5.3 0.3 5.4         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Arp 299-A| 41.86 0.04 41.87 6.5 0.2 6.4         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 1068 | 41.38 0.08 41.33 7.7 0.2 7.8         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 1365-SW | 41.48 0.07 41.49 5.9 0.4 5.3       |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 1365-NE| 41.10 0.07 40.97 5.8 0.6 4.9         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 4038 | 40.62 0.37 40.79 7.5 1.1 8.5         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 4038 (Overlap) | 40.69 0.44 40.79 6.2 0.9 6.0       |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Mrk 231  | 42.07 0.2 42.10 6.8 0.3 6.6         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Arp 299-B| 40.44 0.11 40.43 6.6 0.3 6.8         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Arp 299-A| 40.19 0.09 40.17 5.8 0.3 5.0         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 253  | 40.78 0.12 40.73 6.3 0.2 6.6         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| NGC 1266 | 41.25 0.05 41.22 6.8 0.2 6.9         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |
| Cen A    | 40.02 0.05 40.08 5.7 0.3 5.5         |                                  |                                       |                          |                          |                          |                                       |                                    |                                    |                                    |                                  |                                    |

Notes. Luminosities and masses may be lower limits for significantly extended galaxies; all luminosities and masses are those contained in a 43′5 beam.

one-to-one correspondence between the CO and H$_2$ components, in addition to doubts about the LTE approximation for the S(7) and S(5) lines, and the knowledge that the H$_2$ cannot probe the coolest gas anyway. More importantly, fixing the mass of Component III orders of magnitude lower than the other components (to match H$_2$) would produce the same result: a SLED described by the other two components, where the temperature of Component II would simply move up or down (allowable due to the $n−T$ degeneracy) based on the imposed constraints to preserve the same pressure. This was our best-fit result without requiring that the $M_{\text{HI}}$ be orders of magnitude lower than $M_{\text{HI}}$, only that it be lower. The best-fit SLED was statistically indistinguishable from the best-fit two-component SLED (same total $\chi^2$) because the third component contributed negligible flux to each line. We ran the three-component fit again, this time not requiring that $M_{\text{HI}}$ be lower than the other masses (only that the sum be less than the dynamical mass prior, as before). We still found the equivalent of a two-component fit, with the remaining component contributing negligible mass and luminosity.

One could undoubtedly find a good fit to the SLEDs using any number ($\geq 2$) of distinct components. Though the addition of more components perhaps becomes closer to the real situation of a continuous distribution of conditions, the uniqueness of the parameter solutions significantly decreases, and thus the physical parameters themselves become less well constrained. We point out the three-component models end up indistinguishable from the two-component models not because the two-components are the “right” answers, for the reasons discussed in Section 4.1.1, but because the three-component models do not improve the
quality of the fit and cannot be constrained (a wide range of combinations of parameters could reproduce the SLEDs).

4.1.3. Two- versus One-component (Low-J Only) Modeling

How does simultaneously modeling two components change our understanding of the cold component? To answer this, we also ran single-component likelihoods using only the $J = 1 → 0$, $J = 2 → 1$, and $J = 3 → 2$ lines, if all three were available in the literature (for 17 of our 21 pointings, those with green dashed SLEDs shown in Figure 8), allowing for multiple measurements for each line.

We found that the luminosity of cold CO and thermal gas pressure in the cold component was overestimated when modeled alone (using only $J = 3 → 2$ and below) by an average of 0.5 and 0.6 dex, respectively. No effect on the temperature and density could be determined because these two parameters were not as well constrained as the pressure (this is a consequence of their degeneracy in excitation modeling and not specific to the methods compared here). In all cases, modeling only the cold CO will severely underestimate the total CO luminosity, which is dominated by warm gas. The parameter that was usually correctly determined is the CO mass because it is most highly dependent on the $J = 0$, 1, and 2 population levels. This point will become very important when discussing luminosity-to-mass conversion factors in Section 4.2.

Though low-$z$ galaxies are often modeled with low-$J$ lines, high-redshift submillimeter galaxies (SMGs) are often detected in only a few mid-$J$ lines. Carilli & Walter (2013) reviewed studies of cool molecular gas in high-$z$ galaxies and found that quasars require a high-excitation component, related to the AGN, to explain mid-$J$ line flux. We showed that even galaxies with no AGNs require a high-excitation component. Furthermore, they note that SMGs (in contrast with quasars) demonstrate less excited molecular gas and excess emission in the CO $J = 1 → 0$ transition. We have demonstrated that the problem is perhaps best approached from another direction: the “excess” emission is not in the CO $J = 1 → 0$ transition. Instead, the CO $J = 1 → 0$ should be considered as entirely emitted by the coldest gas, and the real excess is in the mid-$J$ lines, requiring the higher-excitation component. Just such a component was found using the $J = 3 → 2$ to $J = 9 → 8$ lines of the $z = 2.56$ Cloverleaf quasar (thermal pressure $> 10^6$ K cm$^{-3}$; Bradford et al. 2009). One cannot disentangle this question without a more complete SLED, as we show here for a range of low-$z$ galaxies (with and without AGNs, with varying degrees of star formation). By more complete, we mean a good distribution of lines from $J = 1 → 0$ to $J = 9 → 8$ or higher. Moreover, the

| FTS Name | $log \frac{L_{\text{warm}}}{L_{\text{cool}}}$ Mean | $log \frac{L_{\text{warm}}}{L_{\text{cool}}}$ σ | $log \frac{L_{\text{warm}}}{L_{\text{cool}}}$ Best |
|----------|----------------|----------------|----------------|
| Mrk 231  | 1.9            | 0.2            | 2.1            |
| IRAS F17207-0014 | 1.2          | 0.2            | 1.1            |
| Arp 220  | 1.2            | 0.4            | 0.9            |
| Mkr 273  | 1.7            | 0.3            | 2.0            |
| UGC 05101 | 1.6           | 0.5            | 1.2            |
| NGC 6240 | 1.2            | 0.2            | 1.3            |
| Arp 299-C | 1.2           | 0.6            | 0.7            |
| Arp 299-B | 1.9           | 0.6            | 1.2            |
| Arp 299-A | 2.0           | 0.3            | 2.1            |
| NGC 168  | 0.6            | 0.2            | 0.4            |
| NGC 1365-SW | 1.2            | 0.5            | 1.0            |
| NGC 1365-NE | 0.7            | 0.3            | 0.4            |
| NGC 4038 | 0.4            | 0.4            | 0.3            |
| NGC 4038 (Overlap) | 0.4        | 0.4            | 0.3            |
| M82      | 1.1            | 0.5            | 0.7            |
| NGC 1222 | 1.3            | 0.4            | 0.7            |
| M83      | 1.6            | 1.0            | 1.5            |
| NGC 253  | 1.5            | 1.1            | 0.7            |
| NGC 1266 | 1.6            | 0.4            | 1.3            |
| Cen A    | 1.3            | 0.3            | 1.6            |
| Weighted Average | 1.2        | 0.1            | 1.8            |

Note. IRAS 09022-3615 is not included because only one component was modeled.

| FTS Name | $T_\text{ex}$ (K) | $σ$ (K) | $M_\text{C}$ (10$^4$ $M_\odot$) | $σ$ (10$^4$ $M_\odot$) |
|----------|-----------------|---------|---------------------------------|-------------------|
| IRAS F17207-0014 | 24             | 5       | 350                             | 30                |
| IRAS 09022-3615 | 20             | 3       | 800                             | 70                |
| Arp 220   | 24             | 5       | 190                             | 20                |
| Mkr 273   | 23             | 3       | 230                             | 10                |
| NGC 6240  | 44             | 6       | 300                             | 20                |
| Arp 299-C | 28             | 4       | 41                              | 1                 |
| Arp 299-B | 27             | 4       | 41                              | 2                 |
| Arp 299-A | 35             | 6       | 52                              | 2                 |
| NGC 1068  | 28             | 1       | 31                              | 0.9               |
| NGC 1365-SW | 25            | 1       | 27                              | 1                 |
| NGC 1365-NE | 24            | 1       | 32                              | 1                 |
| NGC 4038  | 35             | 10      | 4.4                             | 0.4               |
| NGC 4038 (Overlap) | 23          | 1       | 13                              | 0.5               |
| M82       | 36             | 3       | 3.9                             | 0.1               |
| M83       | 39             | 4       | 1.6                             | 0.07              |
| NGC 253   | 33             | 2       | 4.5                             | 0.1               |
| NGC 1266  | 30             | 4       | 11                              | 0.4               |
| Cen A     | 50             | 6       | 0.86                            | 0.05              |
| Average   | 26             | 8       |                                 |                   |
mass estimated from mid-\(J\) lines alone will be an underestimate of the total molecular mass if CO \(J = 1 \rightarrow 0\) is unavailable. We tested the extent of this effect by modeling only the \(J = 3 \rightarrow 2\) to \(J = 6 \rightarrow 5\) lines as one component of molecular gas. On average, the log of the ratio of cold component mass (from our two-component models) to these mid-\(J\) masses was 0.56 ± 0.34. This means masses using mid-\(J\) lines will be underestimated by a factor of 1.7–7.9, or 3.6 on average. For example, with ALMA, the \(J = 1 \rightarrow 0\) (\(J = 2 \rightarrow 1\)) line is unavailable above \(z = 0.4\) (1.7), so it will be difficult to accurately estimate molecular mass.
Table 24

[C II] Line Measurements: 10^{-16} W m^{-2}

| FTS Name       | [C II] | $\sigma$ | % Ionized$^a$ | $\sigma$ | % Ionized$^b$ | $\sigma$ |
|----------------|--------|----------|--------------|----------|--------------|----------|
| Mrk 231        | 3.70   | 0.20     | 20.0         | 3        | 35.0         | 5        |
| IRAS F17207-0014 | 6.70   | 0.80     | 12.0         | 2        | 20.0         | 3        |
| IRAS 09022-3615 | 6.69   | 0.22     | 12.0         | 1        | 21.0         | 2        |
| Arp 220        | 9.40   | 0.40     | 30.0         | 7        | 52.0         | 10       |
| Mrk 273        | 5.50   | 0.30     | 17.0         | 2        | 29.0         | 3        |
| UGC 05101      | 5.59   | 0.28     | 26.0         | 2        | 44.0         | 4        |
| NGC 6240       | 27.2   | 0.60     | 15.0         | 0.5      | 25.0         | 0.9      |
| Arp 299-C      | ...    | ...      | ...          | ...      | ...          | ...      |
| Arp 299-B      | ...    | ...      | ...          | ...      | ...          | ...      |
| Arp 299-A      | 82.2   | 1.2      | 5.3          | 0.3      | 9.1          | 0.5      |
| NGC 1068       | 214    | 1.7      | 20.0         | 0.5      | 35.0         | 0.8      |
| NGC 1365-SW    | 104    | 2.5      | 22.0         | 0.6      | 38.0         | 1        |
| NGC 1365-NE    | 104    | 2.5      | 18.0         | 0.5      | 31.0         | 0.8      |
| NGC 4038       | 50.2   | 1.3      | 6.7          | 0.3      | 11.0         | 0.5      |
| NGC 4038 (Overlap) | ...  | ...      | ...          | ...      | ...          | ...      |
| M82            | 1320   | 4.3      | 8.0          | 0.06     | 14.0         | 0.1      |
| NGC 1222       | 24.2   | 0.90     | 4.2          | 0.2      | 7.2          | 0.4      |
| M83            | 181    | 3.5      | 15.0         | 0.3      | 25.0         | 0.6      |
| NGC 253        | 499    | 5.2      | 8.7          | 0.5      | 15.0         | 0.8      |
| NGC 1266       | 5.00   | 1.0      | 18.0         | 0.4      | 31.0         | 8        |
| Cen A          | 295    | 2.1      | 4.2          | 0.05     | 7.2          | 0.09     |
| Median         | ...    | ...      | ...          | ...      | ...          | ...      |

Notes. All are from Brauher et al. (2008) except UGC 05101 and IRAS 09022-3615 from Díaz-Santos et al. (2013). [N II] line fluxes were given in Table 5.

$^a$ Calculated using [C II]/[N II] ratio = 2.5 in ionized medium.

$^b$ Calculated using [C II]/[N II] ratio = 4.3 in ionized medium.

Figure 14. H$_2$ excitation diagrams. For each line flux available, the total number of molecules is calculated by the equations in Section 3.3. The inverse of the solid line slopes are the excitation temperatures; the S(3), S(2), and S(1) generally lie on a fairly constant line, but the higher and lower energy fluxes demonstrate a gradient in excitation temperatures. The non-extinction-corrected lines are shown in gray.
mass at high redshift. The SLEDs shown here could also be used as analog for missing lines in future high-z molecular gas modeling.

4.1.4. Iterative versus Simultaneous Two-component Modeling

Having compared the difference between one and two components, it is also useful to examine the effect that simultaneous modeling of an eight-dimensional parameter space has compared to an iterative modeling approach, which has been used in the past (e.g., Kamenetzky et al. 2012; Schirm et al. 2014). This iterative modeling involves first modeling high-J lines alone, above some cutoff such as the $J = 6 \rightarrow 5$ line. The low-J line fluxes predicted by the best-fit model are then subtracted from the measured low-J line fluxes, and the remainder is modeled as the cold component. One can continue alternating between warm and cool components until the two solutions converge. Specific comparisons of the results from iterative versus simultaneous modeling are given in Appendix A for M82, Arp 220, and NGC 4038.

This approach has three major issues. First, as discussed near the beginning of Section 3, most likelihood analysis codes suitable for a large number of parameters are not well designed to refine the best-fit solution, which can differ significantly from the median parameters. This means that the selection of the model flux to subtract from the measured fluxes for modeling the second component is not representative of the probability distribution function. Second, the choice of where to break the SLED apart for the two component modeling is somewhat arbitrary, introducing an additional prior, or restriction of parameter space. Schirm et al. (2014) illustrated the differences that can be caused by choosing different lines to break the spectrum; they found the statistical ranges of the parameters found for three different choices do not vary significantly in the case of the Antennae galaxy. Third, as a consequence of the previous two drawbacks, iterative modeling uncouples the uncertainties and covariances of the warm and cool components, which falsely lifts some degeneracies in the analysis. We believe that our parameter estimates and uncertainties are a more accurate description of a two-component model, and that future two-component modeling should allow for covariance between the components’ parameters, as we do here.

4.2. Luminosity to Mass Conversion Factors

It is common to use an empirically measured value to convert from CO $J = 1 \rightarrow 0$ luminosity to total molecular mass. For Milky Way clouds, this is the “X-factor” in units of cm$^{-2}$ (K km s$^{-1}$): $X$(CO) = $N$(H$_2$)/$I$(CO), where $I$(CO) = $\int Tdv$. For extragalactic work, one cannot resolve individual clouds, but an ensemble of emitting clouds would have a similar proportionality known as $\alpha_{\text{CO}} = M/L_X$ (in the respective units given above). However, for an X-factor in terms of $N_H$ (standard) and masses in total molecular gas (including He), the conversion is $X$(CO) = $4.5 \times 10^{19}$/$\alpha$ due to the factor of 1.4 in our Equation (2).

Bolatto et al. (2013) discussed the theoretical basis for the CO-to-H$_2$ conversion and presented a comprehensive summary of the techniques and results of its measurement for Galactic and extragalactic molecular clouds. A typical X(CO) for the disk of the Milky Way is 2 $\times$ 10$^{20}$ ($\alpha_{\text{CO}} \approx 4$), but for the Galactic center, X(CO) is 3–10 times lower. Normal spiral galaxies have values close to that of the Milky Way disk, whereas starburst galaxies and (U)LIRGS have values X(CO) < 1 $\times$ 10$^{20}$ ($\alpha_{\text{CO}} < 2$). For these highly excited galaxies, the lower X(CO) values are often attributed to higher gas temperatures and large velocity dispersions (in excess of self-gravity, see simulations by Narayanan et al. 2011). Additionally, if the CO emission is extended and not confined in self-gravitating molecular clouds, X(CO) would also be lower, a condition that is likely present for ULIRGS (Bolatto et al. 2013). Other factors may influence the CO-to-H$_2$ conversion factor, such as metallicity and gas-to-dust mass ratio. Lower metallicity or gas/dust ratios will decrease the depth of the CO-emitting layer in molecular clouds, decreasing the CO intensity and increasing X(CO). Additionally, X(CO) is only sensitive to CO-bright gas; we may be missing CO-faint H$_2$ reservoirs of H$_2$ where C$^+$ or C is the dominant form of carbon, instead of CO (see further discussion in Section 4.5). We first present our derived values of $\alpha_{\text{CO}}$ and then discuss the systematic effects that could affect these values (see also Maloney & Black 1988).

The masses and luminosities used to derive $\alpha_{\text{CO}}$ are plotted in Figure 15, and resulting values in Table 25. When we collected multiple measurements of the $J = 1 \rightarrow 0$ line, we used a weighted average (after converting all to a 43.5 beam following Section 2.2). We used the total CO mass (cool and warm components), but point out that $\alpha_{\text{CO}}$ is only reduced by about 10% if only using cold CO mass, though the errors remain roughly the same because they are dominated by the errors of the cold CO mass. As discussed in the previous section, the mass estimate using only the first three lines of CO should be the similar to our estimate derived from the entire SLED. This means we do not differ significantly from previous studies also using radiative transfer models to determine mass for this conversion factor.
Table 25

| FTS Name         | log(αCO) | σlog | αCO   | σ   |
|------------------|----------|------|-------|-----|
| Mrk 231          | −0.6     | 0.1  | 0.3   | 0.09|
| IRAS 017207−0014 | 0.05     | 0.4  | 1     | 1   |
| IRAS 09022-3615  | ···       | ···  | ···   | ··· |
| Arp 220          | −0.3     | 0.4  | 0.6   | 0.5 |
| Mrk 273          | −0.3     | 0.4  | 0.5   | 0.5 |
| UGC 05101        | −0.4     | 0.4  | 0.4   | 0.3 |
| NGC 6240         | −0.5     | 0.2  | 0.3   | 0.1 |
| Arp 299-C        | −0.2     | 0.2  | 0.6   | 0.3 |
| Arp 299-B        | −0.3     | 0.3  | 0.5   | 0.4 |
| Arp 299-A        | −0.3     | 0.4  | 0.5   | 0.5 |
| NGC 1068         | −0.5     | 0.4  | 0.4   | 0.3 |
| NGC 1365-SW      | −0.1     | 0.4  | 0.8   | 0.7 |
| NGC 1365-NE      | 0.5      | 0.2  | 3     | 1   |
| NGC 4038         | −0.2     | 0.3  | 0.6   | 0.4 |
| NGC 4038 (Overlap)| ···       | ···  | ···   | ··· |
| M82              | −0.4     | 0.3  | 0.4   | 0.3 |
| NGC 1222         | −0.2     | 0.4  | 0.6   | 0.6 |
| M83              | −0.2     | 0.4  | 0.6   | 0.6 |
| NGC 253          | −0.05    | 0.4  | 0.9   | 0.8 |
| NGC 1266         | −0.2     | 0.4  | 0.6   | 0.5 |
| Cen A            | 0.5      | 0.4  | 3     | 3   |
| Average          | −0.2     | 0.3  | 0.3   | 1.1 |

Notes. See Section 4.2. IRAS 09022-3615 is not included because the cold gas mass was not modeled. Averages do not include the following duplicate pointings: Arp 299-B, Arp 299-C, NGC 4038, NGC 1365-SW.

The dotted lines in Figure 15 clearly demonstrate that we find αCO < 10 in all cases, and in fact αCO ≤ 1 in all but two cases (both with αCO ≈ 3), Cen A and NGC 1365-NE. NGC 1365-SW, however, shows αCO = 0.8, and we would not expect the two to be dramatically different (or particularly independent, given their close separation relative to the FTS beam size, see Appendix A). The discrepancy is higher for the mass found for NGC 1365-NE. Cen A is often an outlier in this sample; its lower gas excitation and lower mass would in fact lead us to expect a higher αCO for reasons described below. Our derived values match well with those in the literature as summarized by Bolatto et al. (2013), though generally on the lower end of values given, e.g., NGC 1068 (Papadopoulos & Seaquist 1999), NGC 4038 (Zhu et al. 2003), Arp 299 (Sliwa et al. 2012), Mrk 231, NGC 6240 (Bryant & Scoville 1999). We are somewhat lower for M82 (0.4 ± 0.3 versus 1.2–2.4, Wild et al. 1992), NGC 4038 Overlap (0.5 ± 0.5 versus 1.2–2.4, Zhu et al. 2003), and Arp 220 (0.6 ± 0.5 versus 2.4, Scoville et al. 1997).

Even with the two outliers, our best-fit αCO is approximately 0.66 ± 0.48 (X(CO) = 0.26 ± 0.21 × 10^20). This is on the low, but not overlapping end of the range of estimates by Yao et al. (2003) for starburst galaxies (X(CO) = 0.3 ± 0.8 × 10^20) and Papadopoulos et al. (2012) for LIRGS (X(CO) = 0.3 ± 10^20). If we instead fit a line to Figure 15, allow for slope not equal to one, we find M = 1312(L^0.65, which corresponds to αCO from 1.9 to 0.4 over the approximate range of L = 10^6–10^10 (K km s^−1 pc^3). The bootstrapped estimate of the slope is 0.68 ± 0.18. This fit is largely fixed by the very low mass error bars on NGC 6240; excluding this point, the linear fit is M = 55(L^0.80, αCO from 1.5–0.6. Here the bootstrapped slope is 0.79 ± 0.18, so we cannot rule out a linear relationship.

A variety of systematic effects could change our derived αCO. First, using a factor of 1.36 (correcting for helium only, as is often done), rather than 1.4 would lower αCO by only a few percent. A different value of the relative abundance of CO to H₂ (not the same as X(CO) in this section) would also modify our mass calculation. We use 3 × 10^-4; another commonly used value, 1 × 10^-4, would lower αCO by a factor of three.

We confirm that a conversion factor αCO < 1 is appropriate for CO J = 1 → 0 emission from LIRGS and other submillimeter-bright local galaxies. This factor may not scale linearly with CO J = 1 → 0 luminosity. We attempted to discern a similar relationship between the CO J = 6 → 5 emission and the warm molecular mass, but did not find one. This is not particularly surprising; the theoretical basis for αCO relies on CO J = 1 → 0 being thermalized and T_{kin} being the same in all sources (Maloney & Black 1988). We find very subthermal excitation in the J = 6 → 5 line (T_{excitation} ≪ T_{kin}). The best-fit excitation temperatures for the CO J = 6 → 5 line range from 3–30 K (with one, IRAS 09022-3615 at 140 K), while the kinetic temperatures are 200–3000 K, and the two are not correlated. Even if the J = 6 → 5 line were thermalized, the warm gas temperature varies in a non-systematic way from galaxy to galaxy. Thus, CO J = 6 → 5 is a poor tracer of mass (but a good tracer of warm component luminosity, as we show in Section 4.4).

4.3. Gas-to-dust Mass Ratios

In Figure 16, we show the dust mass versus the molecular gas mass (for both warm and cold components). For comparison, we also show the 1:1, 10:1, and 100:1 gas:dust mass ratios with dotted lines. Our mean results (for the cold component of CO) lie between the 10:1 and 100:1 lines; the blue best-fit line varies from a ratio of 76 at the lowest end to 42 at the higher end, but the uncertainty in the slope is high enough that we cannot rule out a constant ratio (a linear dust-to-gas relationship). (Recall that the warm mass is generally only 10% of the contribution to the total molecular gas, but that our conclusions utilizing the cold component below are uncertain by a larger factor.)

In a survey of 14 galaxies with the Submillimeter Array (half of which are in this sample), the average gas/dust ratio in the center of galaxies was found to be about 120 ± 28, though with large variation (Wilson et al. 2008, hereafter W08).
The gas/dust mass ratios derived from total galaxy luminosities (comparable to this work) showed even greater variation, with ratios from 29 to 725. Our ratios vary from about 10–120, with considerable error bars, but we do not find ratios in the hundreds. Our estimates for the dust and gas mass are both calculated differently than in W08, where the gas mass was calculated from the CO $J = 3 \rightarrow 2$ flux, assuming an area-integrated luminosity ratio of $(J = 3 \rightarrow 2/J = 1 \rightarrow 0)$ of 0.5 and $\kappa = 0.8$ (recall Section 4.2). For all our available $(J = 3 \rightarrow 2/J = 1 \rightarrow 0)$ line ratios, we find a median of 0.7 and a standard deviation of 0.4. The dust mass in W08 was calculated by scaling the 850 or 800 $\mu$m fluxes to 880 $\mu$m using $\beta = 1.5 \pm 0.5$ and $\kappa = 0.9$ cm$^2$ g$^{-1}$. When our ratios of gas/dust are different, half the time it is due to the dust mass being very different, and the other half of the time, the gas mass.

Our molecular masses are determined by non-LTE modeling, and our dust masses from full SED modeling; we believe these methods to be more robust, and thus rule out gas/dust masses much greater than 120, our largest ratio. This is lower than that of the local region of the Milky Way (140; Draine et al. 2007).

Rény-Ruyer et al. (2014) found that metallicity was the most important parameter in determining gas/dust mass ratios. According to their broken power law model, gas/dust ratios of 1, 10, and 100 correspond to metallicities of 2.2, 1.2, and 0.2 dex above solar. Gas/dust ratios above $\sim 160$ indicate subsolar metallicity. Our ratios, ranging from 76 to 42, would correspond to metallicities of 0.3 to 0.6 dex above solar, increasing with far-infrared luminosity (and proportionally, SFR). Their relationship (which they note is derived from data with considerable scatter), and our data points, are not sufficient to determine the metallicity of individual galaxies with precision.

4.4. Molecular Gas Properties in Context: Comparisons among Galaxies

An examination of the SLED shapes in Figure 5 shows the variety of excitation conditions present in our sample. Some have bright mid-$J$ excitation but turn over at high-$J$ (e.g., M82, NGC 253). Others remain somewhat flat at high-$J$ (e.g., Mrk 273, Mrk 231). On one extreme end, the CO $J = 10 \rightarrow 9$ luminosity of NGC 6240 is over 240 times that of $J = 1 \rightarrow 0$, while for Cen A, the ratio is less than 6.

Having derived a variety of molecular gas properties for the warm and cool components (most reliably luminosity, pressure, and mass), we now examine which of those properties are shared among the sample and which vary with, for example, galaxy $L_{FIR}$. To examine these relationships, we compared each likelihood parameter against the $L_{FIR}$ derived from the dust modeling. No discernible relationships were found for temperature or density, but pressure is discussed below.

The warm and cold component CO luminosities and masses, perhaps not surprisingly, are proportional to $L_{FIR}$ (Figures 17 and 18); massive/luminous galaxies tend to be more luminous across the electromagnetic spectrum. To determine if this were the only relation we were observing, we also examined the slope of the CO luminosity versus mass for the cold (warm) component, finding a slope of $0.8 \pm 0.3$ ($1.3 \pm 0.2$), consistent with unity. We also looked at the CO luminosity per unit mass for each component versus $L_{FIR}$, and found a slope of $0.4 \pm 0.2$ for the cold component, consistent with zero. For the warm component, we find $0.3 \pm 0.1$, which may imply a non-zero relationship; that is, that the ratio of CO luminosity per mass in the warm component may increase slightly with increasing $L_{FIR}$.

Note that in the two aforementioned figures, the cold and warm components are plotted separately; the total mass/luminosity is dominated by the cool/warm components, respectively. Given the large uncertainties in the slopes, we cannot discern a different relationship between mass (or luminosity) and $L_{FIR}$ for the warm and cold components. The total CO luminosity is about $4 \times 10^{-4}$ $L_{FIR}$ (Figure 17). The luminosity in only the cold component is $(2.3–5) \times 10^{-5}$ $L_{FIR}$. The total CO luminosity is also well correlated with the CO $J = 6 \rightarrow 5$ line luminosity (Figure 19).

A consequence of the aforementioned relationships is that the luminosity-to-mass ratio in the warm component is two orders of magnitude higher than that of the cold component. Additionally, we do not detect any obvious outliers from the luminosity relationships in the AGN-dominated galaxies, though this is a small sample. The two notable outliers in $L_{CO}/L_{FIR}$ in Figure 17, that lie above the trend, are NGC 1266 and NGC 6240, both discussed in Appendix A.

In Figure 12, we show histograms of the warm and cool component pressures in red and blue, respectively. We also plot the pressure histogram for molecular cloud clumps derived from the densities measured from the Bolocam Galactic Plane Survey (BGPS; T. P. Ellsworth-Bowers et al., in preparation), assuming a temperature of 10 K (solid line) or 30 K (dashed line). In addition to the temperature dependence, the BGPS distributions in Figure 12 also depend (linearly) on the dust opacity used to calculate the clump mass and density (Ossenkopf & Henning 1990). The warm component clearly has a higher pressure, independent of those assumptions, meaning it is not like most Galactic molecular clumps (though see the comparisons to Sgr B2 and Sgr A* in Section 4.6).

The bulk of the molecular mass in the Galaxy is in lower pressure ($\sim 10^4$ K cm$^{-3}$) clouds, not clumps. Were we to be simply summing or “counting” Galactic-type giant molecular...
clouds in these galaxies, we would expect the cold CO pressures to be similar; instead, ours are higher. (Recall from Section 4.1.3, our cold pressure is 0.5 dex lower than if we modeled this component alone; simultaneous modeling is not the reason our pressure is higher than Galactic.) This means that the bulk of the molecular gas in this sample of high-SFR galaxies is more energetic (higher thermal pressure, and hence greater thermal energy per unit volume) than the bulk of molecular gas in our Galaxy. Additionally, the bulk excitation may be similar to that of denser Galactic clumps, but this additional interpretation relies on the aforementioned assumptions.

One explanation could be the high cosmic-ray energy densities caused by the higher SFRs in these galaxies (Abdo et al. 2010). Cosmic rays can volumetrically heat the gas, including the dense UV-shielded cores that set the initial conditions for star formation; cosmic-ray-dominated regions (CRDRs) heat the gas to 80–240 K in compact extreme starbursts, closer to the cold component temperatures we find here (Papadopoulos 2010). Even if cosmic rays do not dominate the heating, their influence will still heat the gas more than PDRs alone and will increase the Jeans mass and hence the stellar initial mass function mass scale (Papadopoulos 2010). The higher temperatures in our cool gas component may be a direct feedback mechanism of star formation; not from the UV light of O and B stars, but from cosmic rays.

It could still be that we are summing/“counting” molecular clouds that typically have higher pressures than Galactic clouds; in that case, we would expect the mass and luminosity to increase with increasing galaxy mass or luminosity, but the average pressure to remain the same. Though it is hard to discern a relationship between pressure and luminosity (Figure 20), we find best-fit slopes of 0.53 and 0.41 for the cool and warm components, respectively. The bootstrap method yields errors on these parameters of ±0.27 and 0.12. For the cold component, we cannot exclude a zero slope at the 2σ level, but for the warm component, the bulk average pressure appears slightly correlated with $L_{FIR}$ (to a significance of 3.4σ). This implies that the energetics of the warm component in these galaxies are different, not that we are just viewing “more” of the same molecular gas components with increased $L_{FIR}$. The slight correlation between the luminosity/mass ratio and $L_{FIR}$ for the warm component may also be indicative of this.

Other properties we sought to investigate were the relative ratios between the warm and cool component pressure, mass, and luminosity, shown in Figure 13. We did not detect any trend with $L_{FIR}$ (or SFR), the presence of an AGN, $L_{CO_{tot}}$, or dust mass. On average, the log ratios of the warm/cold CO pressure, mass, and luminosity were 1.8 ± 0.2, −1.0 ± 0.08, and 1.2 ± 0.08. Linearly, these correspond to ratios of 60 ± 30, 0.11 ± 0.02, and 15.6 ± 2.7. The pressure is the least well determined ratio. It is dependent upon the relative shapes of the SLEDs of the two components; they can “trade off” a significant amount in the mid-J lines and still fit the overall shape. We find that the two components are not in pressure equilibrium; once equilibrium is not enforced, we have no expectation for what the ratio should be. Aside from the broad constraints that the gas be both dense enough and cool enough to be molecular, but not so dense and cold that the timescale for

Figure 18. CO modeling likelihood results vs. $L_{FIR}$: mass, log(M$_{H_{2}\text{, cool}}$) = (0.34 ± 0.3)log($L_{FIR}$) + (5.3 ± 4), log(M$_{H_{2}\text{, warm}}$) = (0.70 ± 0.1)log($L_{FIR}$) + (−0.4 ± 1.6). Diamonds are medians with 1σ error bars, asterisks are best fits, red/blue represents warm/cold components, and lighter colored points are duplicate galaxy pointings excluded from line fitting.

(A color version of this figure is available in the online journal.)

Figure 19. CO modeling likelihood results vs. $L_{CO_{tot}}$: total CO luminosity, log($L_{CO_{tot}}$) = (0.76 ± 0.13)log($L_{CO_{6-5}}$) + (1.9 ± 1), log($L_{CO}$, warm) = (0.90 ± 0.10)log($L_{CO_{6-5}}$) + (2.2 ± 1). Diamonds are medians with 1σ error bars, asterisks are best fits, red/blue represents warm/cold components, and lighter colored points are duplicate galaxy pointings excluded from line fitting.

(A color version of this figure is available in the online journal.)
we see such different excitation among galaxies, as described in the previous paragraph, we would also expect different distributions of excitation mechanisms within galaxies. The mass and luminosity are global properties (a sum), whereas the pressure is a local quantity (here, an average). Mass and luminosity are anchored by the lowest-\( J \) (for cool) and highest-\( J \) (for warm) lines. This reaffirms previous conclusions in the literature, from studying individual galaxies, that the low-\( J \) CO dominates the mass and the high-\( J \) CO dominates the luminosity and hence the cooling (e.g., Kamenetzky et al. 2012; Rangwala et al. 2011; Spinoglio et al. 2012; Rigopoulou et al. 2013).

4.5. Carbon in Various Forms: C, C\(^+\), CO

Near newly formed, bright O and B stars, CO only exists where it is adequately shielded from dissociation by UV photons. In the traditional model of a molecular cloud, this will be in the interior of the cloud, surrounded by a transition layer in which carbon is mostly neutral and atomic, but the hydrogen is still substantially molecular, and then another layer in which the carbon is mostly ionized and the hydrogen atomic (Hollenbach & Tielens 1997). The molecular gas in the transition layer will not be traced by CO emission, so it is referred to as “CO-dark.” The PDR models of Wolfire et al. (2010) indicate CO-dark gas may account for 30% of the molecular gas mass. New observations indicate that a significant fraction of molecular gas in the Milky Way is CO-dark (Pineda et al. 2013). Here we compare the view of galaxies studied with C, C\(^+\), CO, and dust.

We first discuss the column density ratios (and overall relative abundances) of C, C\(^+\), and CO. Our beam-averaged column densities for the cold and warm components of CO are presented in Table 19, and the total mass from \([\text{C} \text{II}]\) in Table 21. Though we could not calculate excitation temperatures for \([\text{C} \text{II}]\) to use in the equations in Section 3.3, we used 150 K, which corresponds to a fraction of atoms in the upper state of 0.52 (the fraction approaches 2/3 for \( T \gg 92 \) K). Even with this assumption, the uncertainties in the column density ratios are dominated by the uncertainties in the CO column densities. The distributions are shown in Figure 21; we found a median \( N_C/N_{\text{CO}} \sim 0.5 \) and a median \( N_{C^+}/N_C \sim 0.5 \). Almost all \( N_C/N_{\text{CO}} \) values are less than 1, in line with those reported in Wilson (1997), except for NGC 6240, which appears to have \([\text{C} \text{II}]\) emission even more abnormally luminous than its CO emission. There is large dispersion in these ratios.

We next turn our attention to the temperatures derived from the two neutral atomic carbon lines in our spectra. The excitation temperatures of \([\text{C} \text{II}]\), shown in Table 21 appear to be clustered between 20–40 K, regardless of galaxy, and are not correlated to other measures, such as total infrared luminosity, cold CO temperature, or dust temperature (Figure 22). Without correcting fluxes for the dust absorption, which affects the \( J = 2 \rightarrow 1 \) line slightly more than the \( J = 1 \rightarrow 0 \), the derived temperatures would be about 0.5 to 5 K lower. We found an average temperature of 26.3 \( \pm 9.2 \) K, in agreement with the 29.1 \( \pm 6.3 \) K cited for a sample of high-\( z \) galaxies (Walter et al. 2011). This indicates that neutral C is likely tracing the same cool component of gas across a range of galaxy luminosities and redshifts, and is therefore not a particularly good distinguisher of excitation conditions.

However, Papadopoulos & Greve (2004) proposed using the \([\text{C} \text{II}]\) \( J = 1 \rightarrow 0 \) line to measure global molecular gas mass, finding good agreement with molecular mass measured by CO. We also found a correlation between neutral C mass and molecular mass measured from CO, consistent with a linear

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**Figure 20.** CO modeling likelihood results vs. \( L_{\text{FIR}} \): pressure, \( \log(P_{\text{cool}}) = (0.5 \pm 0.3)\log(L_{\text{FIR}}) + (-1.4 \pm 3.4) \), \( \log(P_{\text{warm}}) = (0.4 \pm 0.1)\log(L_{\text{FIR}}) + (2.1 \pm 1.4) \). Diamonds are medians with 1\( \sigma \) error bars, asterisks are best fits, red/blue represents warm/cool components, and lighter colored points are duplicate galaxy pointings excluded from line fitting. (A color version of this figure is available in the online journal.)

**Figure 21.** Column density ratios of C, C\(^+\), CO. Top panel is the ratio of C\(^+\) to C column density, bottom panel is ratio of C to CO column density. Duplicate pointings of galaxies are not filled in by diagonal lines. The only galaxy not included in the bottom plot is NGC 6240, with an abnormally high ratio of 38.
We determined the populations of the share (NGC 6240, Arp 220, and Mrk 231). We differed in how we required a higher average abundance of [C i] to match our measured [C i] mass. We confirm the conclusions of Papadopoulos & Greve (2004). In the end the population levels were roughly the Boltzmann distributed populations, as opposed to using one line. We have already discussed some differences between our galaxies and the Milky Way; can these distributions be valid in starburst galaxies? In Section 3.5 and Table 24, we presented the estimated percentage of C+ emission from ionized gas using line ratios, and found that in most cases, the fractions are higher than 4%, with a median of 14%–25%. They are not correlated with $L_{\text{IR}}$ or [C i]/$L_{\text{IR}}$. This matches with the 27% (error range 19%–46%) found for the Carina Nebula (Oberst et al. 2006). However, we cannot say anything about the distribution of the remaining source contributions, only that there is less (proportional) [C i] line emission from the sum of PDRs, CO-dark H$_2$ gas, and cold atomic gas in these galaxies than in the Milky Way. Pineda et al. (2013) found that the fraction of mass from CO-dark H$_2$ increases with Galactocentric distance, from 20% at 4 kpc to 80% at 10 kpc. Because the emission from our galaxies is more akin to that of the Galactic center, we expect lower fractions of CO-dark H$_2$ gas than in the Milky Way as a whole. A study similar to that of Pineda et al. (2013) and Langer et al. (2014) could be conducted for the nearest galaxies or Milky Way satellites comparing the distribution of HI, C +, $^{12}$CO and $^{13}$CO, and possibly applied to this sample of galaxies.

Even absent formal modeling of PDRs, we see a picture that contradicts traditional PDR models, even with additional heating from mechanical turbulence or enhanced cosmic rays (e.g., Wolfe et al. 2010). Detailed studies of individual galaxies have consistently found that PDR models cannot explain the large luminosities in the mid- to high-J CO lines: Arp 220 (Rangwala et al. 2011), M82 (Kamenetzky et al. 2012), M83 (R. Wu et al., in preparation), NGC 6240 (Meijerink et al. 2013), Cen A (Israel et al. 2014), NGC 891 (Nikola et al. 2011), and the Galactic center (Bradford et al. 2005). In only a few instances
have PDRs been found to be adequate, namely the Antennae (Schirm et al. 2014), IC324 (Rigopoulou et al. 2013), and the outer star-forming ring of NGC 1068 (Spinoglio et al. 2012). Additionally, the low α CO we find requires some combination of higher temperatures (thereby raising the emissivity provided the line remains optically thick) or non-virialized molecular clouds. CRDRs could explain the elevated CO temperatures (Papadopoulos 2010) or be combined with PDRs (Meijerink et al. 2011), which would imply a higher Jeans mass as a consequence. The concurrence of evidence presented here (and in the cited literature) confirms that high-J CO emission is generally powered by non-radiative processes, a conclusion that future models must take into account.

4.6. Comparison to the Galactic Center: Sgr A* and Sgr B2

We have already compared our pressure distributions to those of molecular clumps in the Galactic plane (Section 4.4). Two specific regions in the Galaxy are more comparable to the galaxies in our sample: the warm gas and dust heated and ionized by the massive stars orbiting Sgr A*, and the giant molecular cloud Sgr B2, approximately 120 pc away from Sgr A*. The CO SLEDs of these observations were included in Figure 5.

Goicoechea et al. (2013) found the CO SLED from J = 4 → 3 to J = 24 → 23 in the warm gas within 1.5 pc of Sgr A* was consistent with either a single component of gas (T = 10^{3.1} K, n \leq 10^4 cm^{-3}, \text{ pressure} \leq 10^{1.4} K cm^{-3}) or multiple cooler components at higher density. In the single component case, this hot gas must fill a small fraction of the volume (not homogeneously distributed), and requires excitation in addition to PDRs. Despite its proximity to our Galaxy’s central black hole, the X-ray luminosity is too low to create an XDR, and cosmic rays would only heat the gas to a few tens of K. The authors suggest low-density shocks contribute to the heating of this hot molecular gas, though it is unclear if they are from infalling gas, clump–clump collisions, or outflows from stellar winds or protostars.

Et-xlazure et al. (2013) resolved the three main compact cores, Sgr B2(N), Sgr B2(M), and Sgr B2(S) from the extended envelope of the Sgr B2 molecular cloud in both dust and molecular line emission and absorption. In addition to determining the dust properties over a ~58 arcmin^2 map, they mapped the line emission from the CO J = 4 → 3 to J = 11 → 10 lines. While the J = 6 → 5 warm gas emission is spread over the molecular cloud, that of J = 11 → 10 is highly concentrated around the compact cores. They conduct non-LTE modeling of the CO emission for the B2(N) and B2(M) cores and require two components (starting from the J = 4 → 3 line, not J = 1 → 0), which they denote as warm extended emission (60 and 100 K) and hot compact emission associated with the cores (360 and 320 K). The log(pressure) for the warm components are 6.8 and 7.4, and for the hot components, 8.7 and 8.5, respectively, for B2(N) and B2(M). For our galaxy-averaged spectra, the pressures for our warm component are consistent with those of the Sgr B2 extended molecular cloud emission, and lower than that of the hot components.

While very high molecular gas temperatures are not found in the Galactic plane as a whole, they are found in Sgr B2 and Sgr A*. Though we cannot resolve molecular clouds in nearby galaxies, it is clear that the high-J lines are emitted from regions of highly excited gas. As one progresses from lower to higher J, the area filling factor of the emitted region becomes progressively smaller, as was demonstrated by Et-xlazure et al. (2013) for Sgr B2. The SLEDs of the Sgr B2 cores, shown in Figure 5, peak at higher-J than the mid-J peak of the extended Sgr B2 molecular cloud envelope (which is more similar to our galaxies). This means that our warm component emission is likely dominated by regions resembling the warm extended molecular cloud envelopes (whose pressure matches those we measure here), not star-forming cores (of a higher pressure). While such compact regions are undoubtedly present, it must be at a lower level, so the bulk of the emission we measure is from the extended molecular clouds, not cores. We tested this by examining the total integrated flux of the Sgr B2 SPIRE FTS map, as one would measure if it were a distant point-source. The resulting SLED is similar to that of the Sgr B2 molecular cloud, not the cores, despite their brightness in high-J lines. As discussed in Section 4.1.2, we know there are gradients in physical conditions in our SLEDs, as we saw from LTE analysis of H2 lines; the emission from cores (the hottest material) contributes an undetectably small fraction of the total high-J CO emission over the whole galaxy. The broad implications for future modeling are clear: the excitation conditions and the geometries (filling factors) of the mid- to high-J lines are different from, e.g., J = 1 → 0, but not completely independent from one another. ALMA can achieve unprecedented spatial resolution in observations of the J = 6 → 5 line; such information can be used to place further prior information on CO modeling and possibly disentangle the multiple components (e.g., the analog to those seen in the Galactic plane, the Sgr B2 molecular cloud, and the Sgr B2 cores) within nearby galaxies. The PACS instrument onboard Herschel was also able to observe even higher-J lines than SPIRE; Hailey-Dunsheath et al. (2012) was able to detect the even higher-excitation component of gas that lies beyond the SPIRE spectrum in NGC 1068.

5. CONCLUSIONS

We presented spectra of 17 infrared-luminous galaxy systems at 21 different pointings observed with the Herschel FTS from 450–1550 GHz. We have created a uniform, consistent pipeline that can perform analysis of such spectra, including source–beam coupling corrections, line fitting, and an eight parameter likelihood analysis of the warm and cool CO gas for each source. Such analysis for nearby galaxies can, at this time, only be performed with Herschel data, which contain enough CO lines to construct SLEDs up to J = 13 → 12.

Is the highly luminous warm component of molecular gas found in early Herschel SPIRE FTS studies generically present in high-SFR galaxies, and how does its presence modify what we already knew about cool molecular gas? Accounting for the warm gas component luminosities, what L CO/L FIR are observed, and what other properties vary with, e.g., L FIR? We found that high-excitation molecular gas is ubiquitous in this sample of galaxies with log(L FIR) from ~10 to 12.5. We clearly distinguish a low-pressure/high-mass component traced by low-J lines from a high-pressure/low-mass component in all systems from their CO SLEDs. Most of the CO luminosity is emitted from the warmer, high-pressure component; the total CO luminosity is about 4 \times 10^{-4} L FIR, and is well-traced by the CO J = 6 → 5 line. The ratios of the warm/cold pressure, mass, and CO luminosity were 60 \pm 30, 0.11 \pm 0.02, and 15.6 \pm 2.7. Though the molecular gas mass and CO luminosity scale linearly with L FIR, the highly excited molecular gas pressure is proportional to L FIR^{0.4 \pm 0.1}, suggesting higher excitation per bulk mass of molecular material. The total mass of the low-pressure molecular gas is well traced by the CO J = 1 → 0 line (and
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**APPENDIX A**

**NOTES ON INDIVIDUAL GALAXIES**

In this appendix, we discuss both the treatment of extended
galaxy data, when applicable, and compare to previous modeling
results, which when done on an individual basis, often include
more specifics than presented here. To create a reasonable
pipeline for application for a large number of galaxies with
limited supplemental information, we did not include such
information, but notable cases are discussed here. Additionally,
Figure 24 illustrates the position of the FTS beam for the three
galaxies with multiple pointed observations.

**A.1. The Antennae: NGC 4038/Overlap**

This pair of merging galaxies is very extended on the sky
(Figure 24). Our H$_2$ lines come from (Brandl et al. 2009),
which measured the emission at multiple locations in the overlap
region. We use a sum of Peaks 1, 2, 3, and 5 for this region;
S(3) is an upper limit. Only one pointing was measured for the
NGC 4038 nucleus and the Overlap region. Their best-fit CO
SLEDs indicate less warm component emission contribution
to the mid-J lines than ours for NGC 4038, and more for the
Overlap region. This illustrates how an iterative modeling
approach can restrict the allowed parameter space somewhat
artificially, whereas our simultaneous modeling allows for more
possibilities of “trade-off” between the two components. We
recover the same total mass in the cold component (of both), with
smaller uncertainties, though lower pressures (with overlapping
1σ ranges) for NGC 4038. For the warm component, we have
higher uncertainties in the mass (though overlapping
distributions), and lower pressures (only the NGC 4038 pressure
distribution 1σ range overlaps). Recovering the same total
mass, given the similarities of our methods, is very reassuring.
Schirm et al. (2014) also finds consistent [C i] LTE temperatures
of 10–30 K.

**A.2. M82**

For low-J CO lines, we use the measurements from Ward et al.
(2003), which are actually at two separate locations in M82,
separated by ~19′. The correct value of η for their 24′.4 beam
is 0.50, and we then used the photometer maps to determine
the ratio of the flux when centered on the two separate lobes
(Ward’s measurements) to that when pointed at the center (our
measurements). We determined that we should sum the two
fluxes and then divide by 0.29. This is close to the number one
would use if treating the two fluxes as uniformly extended (the ratio of the two beam sizes is 0.32).

A similar CO modeling analysis was done in both Panuzzo et al. (2010) and Kamenetzky et al. (2012), using an iterative approach instead of simultaneous modeling. We find similar results for the cold component pressure and mass, but slightly higher warm component pressure and mass. Our \( \log(P_{\text{warm}}) \) is 6.8 \pm 0.3 compared to 6.6\( ^{+0.2}_{-0.5} \) in Kamenetzky et al. (2012), and \( \log(M_{\text{warm}}) \) is 6.9 \pm 0.3 compared to 6.2\( ^{+0.5}_{-0.2} \). As discussed for the Antennae, we would not expect exactly the same results when both components are allowed to vary against one another.

A.3. NGC 1068

NGC 1068’s geometry poses a unique challenge for the FTS because of the separate emission from the central circumnuclear disk (CND; \( \sim 4'' \) diameter) and the larger star-forming (SF) ring (\( \sim 40'' \) diameter), both of which are contained in the SPIRE beam. Hailey-Dunsheath et al. (2012) found the emission from \( J = 14 \rightarrow 13 \) through \( J = 30 \rightarrow 29 \) contained a clear inflection point, implying two components of medium (\( P = 10^{7.8} \) K cm\(^{-3} \)) and high (\( P = 10^{9.2} \) K cm\(^{-3} \)) excitation; this emission was coming from the central 10\( '' \), with the high-excitation component blueshifted by 80 km s\(^{-1} \). Spinoglio et al. (2012) subtracted the medium-excitation component contribution from the lines in the FTS SSW detector (\( J = 9 \rightarrow 8 \) to \( J = 13 \rightarrow 12 \)), which mainly originate from the CND. The remainder was modeled with RADEX, and the contribution to the lower-\( J \) lines in the SLW were subtracted; that remainder was modeled again with RADEX to describe the SF ring. Their 1\( \sigma \) ranges for the log CPRN pressure were 6.5–6.8, and for the SF ring, 4.3–5.2. The pressure and mass for the SF ring overlaps with our cool component; our warm component is at a higher log pressure (7.7 \pm 0.2) because we model all of the emission through the \( J = 13 \rightarrow 12 \) lines; subtracting the ME component from Hailey-Dunsheath et al. (2012) drove their pressure lower.

In our two-component model, the warm component is likely dominated by emission from the CND, whereas the cool component may include significant contributions from both the CND and SF ring. We note that galaxy-integrated photometry fluxes, used to derive \( L_{\text{IR}} \), dust mass, SFR, and stellar mass, will mask the underlying differences between the molecular gas in the CND and the SF ring, influencing NGC 1068’s place on, e.g., the galaxy main sequence.

A.4. NGC 1266

NGC 1266 is unusual for a few reasons. First, it contains a large concentration of H\(_2\) in its nucleus, but shows no sign of an interaction or merger. Second, Alatalo et al. (2011) found evidence for a large molecular outflow via high-resolution CO spectra; the wings of the lines require a low-amplitude, broad Gaussian to be fit properly. We do not attempt to separate the relative contributions of the central velocity component and outflow in our line fits and modeling, though such work is in progress (J. Glenn et al., in preparation). The possible consequence of our treatment is that the conditions we find may be an average between the conditions of the central and outflow components; they may be distinct from our average.

A.5. Arp 299

The FITS images presented in Figure 2 of Sliwa et al. (2012) were given to us by private communication with the author, such that we could convolve each map up to our 43.5'' beam and determine the integrated flux at each of the three pointings (A, B, and C) for CO \( J = 2 \rightarrow 1 \) and \( J = 3 \rightarrow 2 \).

A.6. Arp 220

Though not an extended galaxy, this merger was examined in a similar fashion by Rangwala et al. (2011), who used additional interferometric information to constrain the source size of both the warm and cool components. Additionally, the line fluxes of the different components were scaled by a different linewidth, and iterative, not simultaneous, modeling was used. Likely as a result of these changes, though we find overlapping distributions for the cold component mass and pressure, we find a higher warm component pressure (1\( \sigma \) range log(\( P \)) = 6.6–7.2 instead of 6.2–6.4), and lower mass (1\( \sigma \) range log(\( M \)) = 8.2–8.6 instead of 8.6–8.8). In Section 4.1.2, we discussed three-component modeling, and present some sample results here for Arp 220 in Figures 25, 26, and 27, explained in the captions.

A.7. Cen A

Centaurus A, the radio source in NGC 5128, is the nearest giant elliptical. The aftermath of a merger, Cen A is notable for its bright, compact CND and extended thin disk (ETD). The Herschel FTS beam is centered on the CND, and thus we are not probing the physical conditions in the ETD. Israel et al. (2014) also examined the CO SLED, [C\( i \)], and [C\( ii \)] emission from the
Figure 25. Sample three-component model results for Arp 220. Left: temperature vs. mass. The red and blue shaded regions around the diamonds indicate the 1σ temperature and mass ranges from the two-component likelihood modeling. The black asterisks are the temperatures and masses derived from molecular hydrogen lines (see Section 3.4 and Table 23). We attempted the three-component modeling described in Section 4.1.2 to see if we could separate the warm CO gas (pink box) into medium and higher temperature components similar to H2. The dark blue, green, and dark red X’s and 1σ error bars denote the three-component modeling results for Components I, II, and III, respectively. The distribution of the three components in temperature and mass now seem qualitatively more similar to that of H2. However, Figures 25 and 26 reveal that Component III is not constrained and negligible to the fit. Component II is fulfilling the same role as the warm component, but was limited to a different temperature. Right: SLED, the solid lines indicate the best-fit solution of the three-component model (Section 4.1.2) for Components I (blue), II (green), and III (red). The dashed lines are the best-fit two-component models for the cool (light blue) and warm (fuchsia) components. The dotted lines are the best-fit three-component models when we remove the $0.5 < \log(T/I_{II}/T_{III}) < 2.3$ constraint. However, the best-fit as well as the median solutions still fall in those temperature ranges. The total SLED (gray) is statistically indistinguishable in all three cases. We emphasize that the best-fit model is only one of many models that can fit the data well (and is not necessarily representative of the likelihood distribution) and readers should not over-interpret the differences in the breakdown of individual components; this is why we examine the full parameter space.

(A color version of this figure is available in the online journal.)

Figure 26. Sample three-component model results for Arp 220: derived parameters. From left to right: CO luminosity, pressure (product of temperature and density), and beam-averaged column density (product of column density and filling factor, proportional to mass, top axis). The dark blue, green, and red lines are the marginalized likelihoods of Components I, II, and III, respectively. The light blue and fuchsia lines are for the cool and warm components of the two-component modeling. Qualitatively, Component I and the cool component are the same, as are Component II and the warm component. Component III is generally unconstrained so long as its mass is low enough that it does not modify the fit.

(A color version of this figure is available in the online journal.)

CND and multiple offset pointings of Cen A. For their central pointing, they normalize the measured emission to that of a 22″ beam and find weak or negligible contribution from the ETD; our observations, with a larger beam, may have more contamination but are still dominated by the CND. By a comparison to CO SLEDs of other well-known galaxies, they note that the falling CO SLED at high-J indicates Cen A has the “coolest” CO ladder. Our large velocity gradient (LVG) modeling can quantify this statement: the warm component of CO in Cen A has one of the lowest pressures in our sample.

Israel et al. (2014) models the $^{12}$CO SLEDs simultaneously with $^{13}$CO using two gas components, but does not present marginalized likelihood distributions, instead opting to present three solutions that match the observed SLED well. Our results are not particularly comparable because we allow kinetic temperatures above 150 K. Limiting the temperature will necessarily require a larger portion (of the mass) of the gas to appear much warmer. They also use PDR/XDR models and note the potential importance of mechanical heating. Their estimate of the mass of the CND, $8.4 \times 10^7 M_\odot$, is about a factor
of two smaller than ours (which is their stated uncertainty); our larger beam area, and possible contamination from the ETD within it, may be responsible for some of the difference. We find the highest value of $\alpha_{\text{CO}}$ in our sample for Cen A, but due to the difference in our mass estimate from Israel et al. (2014), we find this in accordance with that of the Milky Way, not twice the value. Parkin et al. (2014) also investigated atomic fine structure lines using PACS and SPIRE and compared to PDR models; they found that the matching PDR properties implies that Cen A is similar to a normal disk galaxy, despite its unique morphology.

A.8. NGC 6240

Our results wholeheartedly agree with the conclusion of Meijerink et al. (2013), that the CO line luminosity-to-continuum ratio is exceptionally high in this galaxy. They argue, through shock modeling of CO and H$_2$, that a high line-to-continuum ratio is a key diagnostic for shocks. Their LVG models were in preparation at the time of this writing.

A.9. Mrk 231

The CO $J = 9 \rightarrow 8$ line of Mrk 231 seems abnormally low compared to the rest of the SLED. For this spectrum, we are using a version reprocessed with HIPE 9 and off-axis background subtraction, but we find the same low flux with SPG v6.1.0 and SPG v11.1.0. The v6.1.0 spectrum includes more frequency overlap between the SLW and SSW regions; fitting the CO $J = 9 \rightarrow 8$ line from the SLW band yields a higher flux, $652 \pm 68$ Jy km s$^{-1}$. In future versions, however, the $J = 9 \rightarrow 8$ line is not available in the more limited SLW frequency range. We do not use the v6.1.0 spectrum because the background subtraction does not properly match the SLW to SSW, which should happen for a point source like Mrk 231.

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