Very high energy gamma-ray production inside the massive binary system Cyg X-1/HDE 226868

W. Bednarek & F. Giovannelli

1Department of Experimental Physics, University of Łódź, 90-236 Łódź, ul. Pomorska 149/153, Poland
2 INAF - Istituto di Astrofisica Spaziale e Fisica Cosmica - Sezione di Roma, Area di Ricerca CNR di Roma-2, Via Fosso del Cavaliere, 100 - I 00133 Roma, Italy

e-mail: bednar@fizwe4.fic.uni.lodz.pl; franco.giovannelli@iasf-roma.inaf.it

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Abstract. TeV γ-ray emission has been recently discovered by Cherenkov telescopes from two microquasars, LS 5039 and LS I +61°303. This emission is likely to be produced inside the binary system since in both cases variability with the orbital period of the binary has been discovered. In fact, such emission features have been recently predicted by the inverse Compton (IC) e± pair cascade model. In this model, electrons accelerated in the jet develop a cascade in the anisotropic radiation of the massive star. The γ-ray spectra emerging from the cascade strongly depend on the location of the observer with respect to the orbital plane of the binary. Here we apply this model in order to investigate the possible γ-ray emission features from another compact massive binary of the microquasar type, Cyg X-1. We conclude that the observational constraints at lower energies (from MeV to GeV) suggest that the spectrum of electrons injected in the jet is likely steeper than in other TeV γ-ray microquasars. The cascade γ-ray spectrum produced by electrons with such spectrum in Cyg X-1 should be below the sensitivities of the MAGIC and VERITAS class Cherenkov telescopes. However, if the electron spectrum is flatter, then the highest TeV γ-ray fluxes are predicted at ~7 hrs before and after the phase when the compact object is in front of the massive star. We suggest that Cherenkov telescopes should concentrate on these range of phases since the TeV flux can vary by a factor of ~20 with the period of the Cyg X-1 binary system. Moreover, the model predicts clear anticorrelation of the GeV and TeV γ-ray emission. This feature can be tested by the future multiwavelength observations with the AGILE and GLAST telescopes in the GeV energy range and the MAGIC and VERITAS telescopes in the TeV energy range.

Key words. gamma-rays: theory – radiation mechanisms: non-thermal – binary systems: close; individual: Cyg X-1

1. Introduction

The importance of high energy processes in X-ray binary systems has been hypothesized for about two decades and in fact some evidence (although not statistically significant) has been reported in the literature (for review see e.g. Weeckes 1988, 1992). However, only one of these early Cherenkov observations of Cen X-3 has been later confirmed, and remains unquestioned up to the present time (Chadwick et al. 2000, Atoyan et al. 2002). Some of these well known binary systems have been also related to the EGRET sources above 100 MeV due to directional coincidence since they are close or inside of relatively large error boxes of some EGRET sources: LS I +61°303 = 2CG135+01 = 2EG J0241+6119 (Thompson et al., 1995, Kniffen et al. 1997), Cyg X-3 = 2EG J2033-4112 (Mori et al. 1997), Cen X-3 (Vestrand, Sreekumar & Mori, 1997), and LS 5039 = 3EG J1824-1514 (Paredes et al. 2000). However, only very recently some binary systems belonging to the class of high mass binaries, have been explicitly detected at high energy γ-rays by Cherenkov telescopes. The HESS collaboration reported the detection of TeV γ-ray emission from the Be type binary system PSR B1259-63, close to the periastron passage (Aharonian et al. 2005). Also TeV γ-rays have been detected from LS 5039 (HESS collaboration, Aharonian et al. 2005, Aharonian et al. 2006) and LS I +61 303 (MAGIC collaboration, Albert et al. 2006). These two objects belong to the class of the so-called microquasars. These objects show evidences of anisotropic outflows usually interpreted as jet structures similar to the relativistic jets observed in active galactic nuclei. Such jets in microquasars might be created in the inner parts of the accretion disks around compact objects such as a neutron or a solar mass black hole that is accreting matter from the companion star.
In fact, microquasar features, very similar to those observed in LS 5039 and LS I +61 303, are also observed in the well-known object, Cyg X-1. It has been detected by the COMPTEL instrument up to ~10 MeV with a spectrum very close to a power law with differential spectral index 2.6 (McConnell et al. 2000, 2002). However, the source has not been observed at higher energies by the EGRET instrument (see the upper limit in McConnell et al. 2000). The MeV γ-ray emission is usually interpreted in terms of two component thermal and non-thermal comptonization models from the accretion disk (e.g. Gierliński et al. 1999), or as a result of comptonization of the stellar photons by relativistic electrons inside the jet (Bednarek et al. 1990, Georganopoulos et al. 2002, Romero et al. 2002). The general picture of the production of γ-rays is that they arise as the result of comptonization of stellar photons by electrons in the jet. This model has been recently applied to the microquasar LS 5039 (Dermer & Böttcher 2006 and Bosch-Ramon, Romero & Paredes 2006). However, these models do not take into account Inverse Compton (IC) e± pair cascade processes. Cascade processes become important for these binary systems since the optical depth for electrons (which are isotropic in the jet) depends largely on their temporary directions (for detailed calculations of the optical depths, see Bednarek 1997, 2000 and more recently e.g. Sierpowska & Bednarek 2005, Böttcher & Dermer 2005, Dubus 2006, Bednarek 2006a). Due to this effect, electrons lose energy mainly in directions for which the optical depths are the largest, but not in the direction toward the observer (see the previously cited papers). The calculations of the γ-ray spectra, which are produced in the anisotropic IC e± pair cascade toward the observer, and their light curves as a function of the phase of the binary system, have been recently calculated by (Bednarek 2006a). These calculations are based on the previous work done for other compact binary systems such as Cyg X-3 (Bednarek 1997), and Cen X-3 (Bednarek 2000, Bednarek & Giovannelli 1999). Recently, the cascade model for the high energy processes inside compact massive binaries has been successfully applied to the binary system LS I +61 303, predicting the phases at which the maximum TeV γ-ray emission can be expected (Bednarek 2006a, b). Such a prediction was confirmed by MAGIC observations (see Albert et al. 2006). As an alternative scenario, hadronic production of γ-rays and neutrinos from these binaries has been also considered (e.g. Romero, Christiansen & Orellana 2005, and Aharonian et al. 2006).

In view of the recent discoveries of the TeV γ-ray emission from microquasars LS 5039 and LS I +61 303, we consider the IC e± pair cascade model for possible high energy processes in another binary system, Cyg X-1/HDE 226868.

### Table 1. Parameters of the binary system and the jet.

| Parameter | Value |
|-----------|-------|
| $R_*$: stellar radius | 20 $R_\odot$ |
| $T_*$: surface temperature | $3 \times 10^3$ K |
| $M_*$: stellar mass | 40 ± 10 $M_\odot$ |
| $M_\gamma$: companion mass | 16 ± 3 $M_\odot$ |
| $a$: orbital radius | 2.15$R_*$ |
| $e$: eccentricity | 0 |
| $i$: inclination | 30° |
| $r_{in}$: disk inner radius, radius of the jet | 10$^7$ cm |
| $\alpha$: jet opening angle | 0.1 rad |
| $z_{min}$: inner boundary of the active jet | 0.1$R_*$ |
| $z_{max}$: outer boundary of the active jet | 10$R_*$ |
| $\eta$: magnetization parameter of the jet | 1.0-0.01 |
| $B_0$: magnetic field at the base of the jet (for $\eta = 1$) | 10$^5$ G |
| $\xi$: acceleration efficiency of electrons | 0.5-0.01 |

### 2. The binary system Cyg X-1/HDE 226868

Cygnus X-1 has been the most extensively studied stellar mass black hole candidate since its discovery as one of the most intense X-ray sources in the sky (Bowyer et al. 1965). In the X-rays the source shows two emission states (see, e.g. Friedhorsky, Terrell & Holt 1983, Ling et al. 1983, Liang & Nolan 1983), spending most of the time (~90%) in the so-called hard state (low level of soft X-ray emission) and the remaining of the time in the soft state. Cyg X-1 was also identified as a radio source by Braes & Miley (1971). High resolution radio observations show a steady jet from this source in the hard X-ray spectral state (Stirling et al. 2001) and also a radio and optical lobe oriented along the jet direction (Gallo et al. 2005). The jet appears when the X-ray spectrum starts softening and its intrinsic velocity is estimated on $\geq 0.3c$ (Fender et al. 2006).

Hjellming & Wade (1971) identified Cyg X-1 with the optical star HDE 226868, which is an O9.7 Iab type massive star inside a binary system with a period of 5.6 days (Webster & Murdin 1972, Bolton 1972). The main parameters of this binary system have been recently confirmed by Ziolkowski (2005): the mass of the optical companion $M_\star = 40 \pm 10 M_\odot$; its radius $R_\star = 22 \pm 3 R_\odot$; an effective temperature of $T_\star = 30,000 \pm 2,000$ K for a distance to the system $D = 1.8-2.35$ Kpc; and a mass of the compact object $M_\gamma = 16 \pm 3 M_\odot$ which is in an almost circular orbit $e = 0$; with an inclination angle of the binary $i = 33^\circ \pm 5^\circ$. In this paper we adopt the values for the binary system shown in Table 1.

### 3. A microquasar in the compact massive binary

We consider a generally accepted scenario for microquasars, in which electrons are accelerated continuously along the jet. The jet propagates from the compact object along an axis perpendicular to the plane of the binary system. The details of such a general scenario have already been described in Bednarek (2006b). Here we repeat the basic points of the scenario for the sake of completeness. The shock acceleration mechanism is usually accepted as being responsible for the acceleration of the electrons. It is assumed that electrons are injected with
the power law spectrum extending up to the maximum energies determined by the balance between the acceleration rate and the most efficient energy loss rate. In the case of microquasars, the synchrotron process (determined by the magnetic field strength locally in the jet) or the inverse Compton process (determined by the radiation field of the massive star) usually provide the most efficient cooling for the electrons.

The magnetic field strength inside the jet can be estimated on the basis of the equipartition arguments concerning the relation between the accretion disk luminosity and the kinetic power of the jet, i.e. the so called jet-accretion-disk symbiosis model developed by Falcke et al. (1995), Falcke et al. (2004). In fact, in the case of Cyg X-1, the X-ray luminosity (probably produced in the accretion disk) and the jet kinetic power are estimated to be of the same order (Gallo et al. 2005). Note, however, that this is not always the case since some other binaries are clearly underluminous, e.g. LS 5039 and LS I +61 303. Moreover, it is commonly expected, on the basis of the equipartition arguments, that the energy density of the magnetic field inside the jet should be related to the kinetic power of the jet (see e.g. Bosch Ramon et al. 2005).

Therefore, we accept the hypothesis that the magnetic field strength at different parts of the jet, which are above \( z_{\text{min}} \approx 10^{15} \text{ eV} \) inside the Crab Nebula. On the other hand, the theory of shock acceleration processes estimates \( \xi \approx 0.1(v/c)^2 \), i.e. \( v > 0.3c \) (Malkov & Drury 2001). Therefore, in this paper we consider the values of the acceleration efficiency of electrons in the jet in the range \( \xi = 0.5 - 0.01 \). The basic parameters which describe the jet are shown in Table 1.

As we noted above, during the acceleration process, electrons lose energy mainly by the synchrotron and the inverse Compton (IC) processes. We are interested in situations in which electrons can be accelerated to TeV energies. This is not easy to obtain relatively close to the base of the jet where the magnetic field is large and the synchrotron losses very strong. Therefore, since we are interested in efficient injection of high energy IC \( \gamma \)-rays by electrons in the jet, it makes sense to consider distances from the accretion disk for which the IC energy losses on the massive star radiation are at least comparable to synchrotron losses. In this cascade model we will concentrate on the parameter range adequate for the production of TeV \( \gamma \)-rays.

Let us estimate the maximum energies of electrons in the shock acceleration process allowed by the energy losses. In these estimations we concentrate on the parts of the jet which are above \( z_{\text{min}} = 0.1R_{\odot} = 1.4 \times 10^{11} \text{ cm} \), since very close to the base of the jet the radiation field from the accretion disk (and disk corona) may dominate over the massive star radiation field (total luminosity of the disk is estimated in several times \( 10^{37} \text{ erg s}^{-1} \), see e.g. Poutanen, Krolik & Ryde 1997). At \( z_{\text{min}} \), the disk radiation field is diluted by the factor of \( \sim (\beta z_{\text{min}}/r_{\text{in}})^2 \approx 10^{-6} - 10^{-4} \), where \( r_{\text{in}} \approx 10^7 \text{ cm} \) is the inner radius of the disk around the 10\( M_{\odot} \) black hole, and the parameter \( \beta = r_{\text{in}}/r_{\text{cor}} \approx 0.01 - 0.1 \) defines the extend of the disk corona assumed in the range of \( r_{\text{cor}} \approx 10 - 100r_{\text{in}} \). Note that the massive star luminosity in Cyg X-1 is clearly larger than the disk luminosity. Therefore, disk radiation can become important only in a relatively small part of the inner jet.

The energy loss rate by the synchrotron process is given by,

\[
\dot{P}_{\text{syn}}(\gamma) = \frac{4}{3} \pi \sigma_{\text{T}} c U_B \gamma^2 \approx 2.7 \times 10^{-3} B^2 \gamma^2 \text{ eV s}^{-1},
\]

where \( U_B = B^2/8\pi \) is the energy density of the magnetic field, \( \gamma \) is the Lorentz factor of the electrons, and \( \sigma_T \) is the Thomson cross section. Electrons lose energy on the IC process in the Thomson (T) regime, if their Lorentz factors are,

\[
\gamma \ll \gamma_{\text{TN}} = mc^2/3k_BT \approx 2 \times 10^5/T_4,
\]

where \( T = 10^4T_4 \text{ K} \) is the surface temperature of the massive star which defines the black body spectrum, and \( k_B \) is the Boltzman constant), and in the Klein-Nishina (KN) regime, for the Lorentz factors \( \gamma \gg \gamma_{\text{TN}} \). The energy loss rate in the Thomson regime is given by

\[
\dot{P}_{\text{IC}}(\gamma) = \frac{4}{3} \pi \sigma_{\text{T}} c U_{\text{rad}} \gamma^2 \approx 3.8 T_4 \gamma^2 \text{ eV s}^{-1},
\]
where \( U_{\text{rad}} = 4.7 \times 10^{13}T_4^4/r^2 \) eV cm\(^{-3}\), and \( r \) is the distance to the center of the massive star in units of its radius \( R_\star \). The energy loss rate in the KN regime depends only logarithmically on the Lorentz factor of the electrons. We approximate these losses by (see e.g. Blumenthal & Gould 1970),

\[
\dot{\mathcal{P}}_{\text{IC}}(\gamma) \approx \dot{\mathcal{P}}_{\text{IC}}^T(\gamma_{\text{KN}}) \ln \left( 4eB_eT_\gamma/m_e^2 - 2 \right).
\]  

(6)

The maximum energies of the accelerated electrons are determined by the balance between the acceleration mechanism and the most efficient mechanism for the energy losses. The comparison of Eqs. (2) and (3) gives the maximum allowed Lorentz factors of the electrons due to the synchrotron energy losses,

\[
\gamma_{\text{syn}} \approx 6 \times 10^7 (\xi / B)^{1/2}.
\]  

(7)

The maximum energies allowed by the IC process in the Thomson regime are (from Eqs. 2 and 5),

\[
\gamma_{\text{IC}}^T \approx 1.6 \times 10^6 (\xi B)^{1/2} T_4^2/r,
\]  

(8)

and in the KN regime are (from Eqs. 2 and 6),

\[
\gamma_{\text{IC}}^{\text{KN}} \approx 1.5 \times 10^5 (2 + e^{(7 \xi B^2 T_4^2)}/T_4).\]  

(9)

Note that the limit given by Eq. (8) is only valid provided that \( \gamma_{\text{IC}} \approx \gamma_{\text{IC}}^{\text{KN}}, \) i.e. when the parameters of the jet and the massive star fulfill the following condition, \( T_4/r > 8(\xi B)^{0.5} \) (from Eqs. 4 and 8). In any other case, the limit given by Eq. (9) has to be taken.

The Larmor radii of electrons accelerated to the maximum Lorentz factors allowed by the radiation constraints has to be smaller than expected from the constraints imposed by the size of the jet. The Larmor radius of electrons (defined below Eq. 2) is thus lower than the size of the jet, \( r_L < (1 + \alpha z) r_{\text{in}} \) (see above), provided that \( \gamma_{\text{size}} \approx eB_\eta/m_e \). For the considered parameters and the applied model for the magnetic field distribution along the jet (see Eq. 1), \( \gamma_{\text{size}} < 6 \times 10^8 \). Note that this limit is independent of the distance from the base of the jet. It does not impose additional constraints on the values obtained above for distances from the base of the jet which are of interest in this model.

The maximum Lorentz factors to which electrons can be accelerated at a specific part of the jet are determined by the acceleration efficiency and the energy losses through synchrotron and IC processes. These energy loss processes depend on the conditions in the jet (i.e., magnetic field strength and acceleration efficiency), on the parameters of the massive star (its radius and surface temperature), and on the distance of the acceleration region from the massive star. In Fig. 1 we plot the maximum Lorentz factors of electrons as a function of the distance from the base of the jet (given by either Eq. 1 or Eq. 3, or Eq. 9, for selected values of the acceleration efficiency, \( \xi \), and the ratio, \( \eta \). The maximum energies of the accelerated electrons increase with the distance from the base of the jet as \( \propto z^{1/2} \), when the acceleration process is saturated by synchrotron energy losses (see also Bosch Ramon et al. 2006). However, in the regions of the jet where the magnetic field is relatively weak (farther from the base of the jet but still close to the massive star), the acceleration process is saturated by IC energy losses. Then, the maximum Lorentz factors of the electrons are significantly lower (note the broad parabolic dips in Fig. 1, especially evident during the periastron passage of the compact object).

In a previous work (Bednarek 2006b), we have shown that electrons accelerated in the jet have to cool locally, i.e. close the the acceleration site, due to the very large energy losses, provided that they are injected within \( \sim 100 R_\star \).
Fig. 2. (a) The optical depths for γ-rays (as a function of their energy) on e± pair production in collisions with stellar photons calculated for γ-rays propagating from a specific distance from the massive star up to the infinity. γ-rays are injected at three different distances from the massive star HDE 226868, \( z = 2R_\star \) (a), \( z = 5R_\star \) (b), and \( z = 20R_\star \) (c), and for selected angles measured from the direction defined by the centers of the stars, \( \alpha = 0^\circ \) (i.e. toward the center of the massive star), the optical depth is calculated only to the surface of the star, thick full curve), \( 30^\circ \) (thick dotted), \( 60^\circ \) (thick dotted), \( 90^\circ \) (thick dot-dashed), \( 120^\circ \) (thin full), \( 150^\circ \) (thin dashed), and \( 180^\circ \) (thin dotted).

from the base of the jet. At larger distances accelerated electrons are advected outside the binary system (along the jet) and can produce high energy radiation through other processes. However, in such a case, we do not expect any clear variability for the γ-ray emission with the period of the binary system. Therefore, we do not consider that possibility in this paper.

Following our previous work, we also assume that electrons are injected with the power law spectrum described by the single spectral index independent on the distance from the base of the jet \( z \) (typical values from the range 2–2.6 are considered). However, the injection rate of electrons, i.e. the power transferred from the magnetized plasma to relativistic electrons \( L_e \), can differ, depending on a range of possible processes occurring in the jet. Two different likely scenarios are considered:

1. constant injection of electrons along the jet from its base at \( z_{\text{min}}: L_e = \text{const.} \),
2. injection rate drops along the jet according to \( L_e(z) \propto z^{-2} \).

3.1. Propagation of γ-rays

Since the Cyg X-1 binary system is very compact (with a separation of the stars of only \( a = 2.15R_\star \)), γ-rays produced in the part of the jet which is closer than a few tens of \( R_\star \), from the massive star can be efficiently absorbed by collisions with the thermal radiation from the massive star. Following our previous works (Bednarek 1997, 2000, Sierpowska & Bednarek 2005), we calculate the optical depths for γ-rays as a function of the energy in the most general case, i.e. for an arbitrary distance from the massive star and direction of their propagation (for an angle measured from the direction defined by the centers of the stars). The results are shown in Fig. 2 for an injection distance of γ-rays from the center of the massive star at \( 2R_\star \) (a), \( 5R_\star \) (b), and \( 20R_\star \) (c). It is clear that the optical depths are significantly above unity at specific directions even if the injection distance from the massive star is quite large. Since the cross sections for the IC process in the KN regime and for the \( \gamma+\gamma \) collisions (\( \gamma+\gamma \rightarrow e^\pm \)) are comparable, it is expected that relativistic electrons injected isotropically inside the jet lose energy mainly in directions where the optical depths are the largest. They inject primary γ-rays mainly in directions of the largest optical depths, i.e. toward the source of soft radiation. These primary γ-rays can develop IC e± pair cascades in the anisotropic radiation field of the massive star. A part of these cascade γ-rays escape toward the observer located at specific directions with respect to the binary system. We follow such a complicated cascade process applying the Monte Carlo cascade code described in detail in our previous works (e.g. Bednarek 2000, 2006a). The code includes also the effects connected with synchrotron cooling of the electrons injected into the magnetic field of the jet. Therefore, we are also able to calculate the simultaneous synchrotron photon spectra produced by electrons accelerated in the jet. γ-ray photons escaping from the binary system are sorted in specific ranges of solid angles on the hemisphere and grouped at specific ranges of energies. Therefore, as a final product, we obtain the γ-ray spectra produced in such anisotropic cascades at specific directions on the hemisphere.

We note that in parts of the jet relatively close to the accretion disk (this part of the jet is not considered in the present paper), γ-rays can also be absorbed in the disk radiation field (see, e.g., the calculations of the optical depths by e.g. Herterich 1974, Protheroe & Staney 1987, Carraminana 1992, Bednarek 1993). The disk radiation can be also upscattered to the γ-ray energies by electrons provided that they are accelerated very close to the base of the jet as considered by e.g. Aharonian et al. (1985) or Romero et al. (2002).
Fig. 3. Cascade γ-ray spectra produced by electrons injected at different distances from the base of the jet \( z = 0.1 r_\star \) (full curve), \( 1 R_\star \) (dashed), and \( 10 r_\star \) (dotted) for two locations of the compact object on its orbit around the massive star, in front of the massive star (upper figures) and behind the massive star (bottom figures). The γ-ray spectra expected from the jet moving inside the hemisphere containing the observer, who is located at the inclination angle of \( i = 30^\circ \), are shown on the left figures, from the counter-jet (middle figures), and the sum of the jet + counter-jet spectra (right figures). The acceleration of electrons in the jet is defined by the parameters \( \xi = 0.1 \) and \( \eta = 0.1 \) and the electrons are injected with a power which drops along the jet according to \( L_e(z) \propto z^{-2} \).

4. Cascade gamma-ray spectra

We investigate the features of the γ-ray spectra produced in such cascade process as a function of parameters describing the acceleration of electrons in the jet. Since the Doppler factor of the jet is unknown in the case of Cyg X-1 (the lower limit on the jet velocity is \( \sim 0.3c \) – Fender et al. (2006) – and the inclination angle of the binary system is \( i \approx 30^\circ \)), two cases should be considered. When the Doppler factor is low, as e.g. in the case of LS I +61 303 (Bednarek 2006b), then we have to consider the γ-ray spectra produced not only by electrons in the jet (directed toward the observer), but also the γ-rays produced by electrons in the counter-jet (directed in the opposite direction). However, for the relativistic jets with Doppler factor \( D \gg 1 \), it is enough to consider only γ-ray emission from the observer-directed jet since the contribution from the counter-jet is suppressed due to relativistic effects. Below we study the basic features of the cascade γ-ray spectra, i.e. their dependence on the distance from the base of the jet, on specific parameters defining the acceleration of electrons, and their dependence on the phase of the binary system and the spectra at specific phases.

4.1. Dependence on the distance from the base of the jet

Let us at first calculate the γ-ray spectra escaping from the binary system toward an observer located at the inclination angle \( i = 30^\circ \). These γ-rays are produced by electrons at different parts of the jet, and their production is parameterized by the distance from the base of the jet. The parameters defining the acceleration of electrons have been chosen from the center of the range of values specified above (i.e. \( \xi = 0.1 \) and \( \eta = 0.1 \) - see Fig. 1). For easier interpretation of the results, we apply the differential power law spectrum of the injected electrons of the type \( \propto E^{-2} \) (equal power per decade) up to the maximum energies defined by \( \xi \) and \( \eta \). In Fig. 3 we show the cascade-produced γ-ray spectra (multiplied by the energy squared) that are produced by electrons in the jet, the counter-jet, and the sum of both of them, i.e. jet + counter-jet spectra. The upper and lower panels show the spectra which are produced when the compact object is in front of or behind the massive star, respectively. The shape of the γ-ray spectra clearly depend on the injection distance of electrons.

Electrons which are injected closer to the base of the jet are also closer to the surface of the massive star and therefore are immersed in a stronger soft radiation field.
These cascade $\gamma$-ray spectra show a low level of TeV emission, due to the absorption of $\gamma$-rays, and a relatively high level of GeV emission (produced due to the efficient cascading). Significant fluxes of TeV $\gamma$-rays can only be produced in the upper part of the considered jet. The cut-offs in the $\gamma$-ray spectra are determined by the maximum energies of electrons accelerated in the jet. These energies increase with the distance from the base of the jet. The $\gamma$-ray spectra produced toward the observer in the cascade process initiated by electrons in the counter-jet typically show higher GeV but lower TeV emission. This is due to the fact that these $\gamma$-rays arrive to the observer after suffering from a severe cascade process (the angle taken from the direction between the jet-counter-jet axis and the direction toward the observer is much larger). In fact, electrons in the counter-jet barely contribute to the $\gamma$-ray spectrum above $\sim 1 \text{TeV}$. Therefore, the sum of the jet + counter-jet spectra (right figures) is similar to the spectra from the jet with some increase in the GeV energy range due to the counter-jet contribution. The counter-jet only has the effect of changing the normalization of the total escaping spectra in the GeV energy range.

4.2. Gamma-ray spectra integrated along the jet

In Fig. 4 we investigate the dependence of the cascade $\gamma$-ray spectra escaping toward the observer as a function of the parameters defining the acceleration model (see the profiles of the maximum electron energies in Fig. 1). The $\gamma$-ray spectra produced in terms of this model are integrated over the part of the jet extending between $(0.1-10)R_*$, since only from this limited part of the jet can the cascade emission dominate (in the radiation of the massive star) and the $\gamma$-ray emission be correlated with the orbital period of the binary system (as recently discovered in the case of LS I +61 303, Albert et al. 2006).

At distances closer than $0.1R_*$, the energy losses via synchrotron process and scattering of the disk radiation might dominate if all electrons can be accelerated in that region to above $\sim 1 \text{TeV}$. At distances greater than $10R_*$, electrons accelerated in the jet are not able to cool locally in the jet. They are advected at large distances along the jet due to the motion of the plasma inside the jet, where they cool via other processes. Note, also, that scenarios in which the possible production of $\gamma$-rays occurs very close or far away from the base of the jet do not provide an explanation of the correlation of the $\gamma$-ray emission with the orbital period of the binary system.

From a comparison of calculations performed for different parameters, we conclude that strong TeV $\gamma$-ray emission appears for larger values of the acceleration efficiency of electrons in the jet (full and dotted curves in Fig. 4). As expected, the $\gamma$-ray spectra generally cut off at lower energies for the case of less magnetized jets and lower acceleration parameters. This is due to the saturation of electron acceleration at lower energies by IC energy losses in these cases (see Fig. 1). The $\gamma$-ray spectra produced in the cascade initiated by electrons, when the jet is behind the massive star, show a sharp cut off at $\sim 100 \text{GeV}$ due to the efficient cascading for all the considered cases. However, when the compact object is in front of the massive star, the TeV $\gamma$-ray emission can reach the observer with a relatively flat spectrum (spectral index $\sim 2.0-2.5$ above a few 100 GeV) and the flux at a level of $\sim 0.1-0.01$ of the GeV emission. We conclude that the $\gamma$-ray emission produced by electrons in the jet in terms of the considered model has very interesting features which should allow us to explicitly distinguish between different models for the $\gamma$-ray production in massive binaries, e.g. scattering of the disk radiation by electrons in the jet (as considered in the case of active galaxies by, e.g. Dermer & Schlickeiser 1993) or production of $\gamma$-rays far away from the base of the jet (e.g. Atoyan & Aharonian 1999).

4.3. Gamma-ray light curve and phase dependent spectra

Let us now discuss the dependence of $\gamma$-ray emission as a function of the phase of the binary system, where the zero
phase is taken when the location of the compact object is behind the massive star. Since the orbit of the compact object is almost circular, the γ-ray light curves should be symmetrical. We calculate the number of γ-ray photons that escape from the binary system toward the observer located at the inclination angle $i = 30^\circ$, in two energy ranges: the so-called GeV energy range (between 1–10 GeV available for the past EGRET telescope and the future AGILE and GLAST telescopes), and the TeV energy range (>200 GeV) available for the present and future Cherenkov telescopes on the northern hemisphere such as the MAGIC and VERITAS telescopes. As an example, we concentrate on the model defined by $\xi = 0.1$ and $\eta = 0.1$ (the parameters from the center of considered range), and the electron spectrum described by $\propto E^{-2}$, and its power dropping along the jet according to $L_\nu(z) \propto z^{-2}$. The γ-ray light curves (number of photons arriving to the observer in the GeV and TeV energy ranges) are shown in Fig. 5 for the case of γ-ray emission only from the jet (thin curves) and the sum of the emission from the jet + counter-jet (thick curves). The TeV γ-ray light curves should be connected with a flattening of the spectrum above ~200 GeV and vice versa. The contribution of γ-ray emission from the counter-jet has an effect of increasing the GeV γ-ray flux with no effect on the TeV flux. However, due to the higher GeV emission, the relative power in the GeV and TeV energy ranges changes. This has consequences for predicting the TeV flux from the normalization to the GeV (EGRET) observations.

5. The multifrequency spectrum of Cyg X-1

The γ-ray spectrum of Cyg X-1 is in fact very poorly constrained. The spectrum in the soft X-ray state shows the power law tail with the differential spectral index $-2.6$ extending up to ~10 MeV, without evidence of a cut off (McConnell et al. 2000, 2002). However, the jet appears only in the low-hard state, so this emission can be only considered as an upper limit on the MeV γ-ray flux related to the jet. The upper limit at higher energies (> 100 MeV) has been derived (see McConnell et al. 2000), based on the 3rd EGRET catalog (Hartman et al. 1999).
Fig. 6. The multiwavelength spectrum of Cyg X-1 (differential spectrum multiplied by energy squared) is compared with the calculated cascade \( \gamma \)-ray spectra for three acceleration models of electrons in the jet: (1) differential spectral index of electrons \( \propto E^{-\alpha} \) and \( \alpha = 2 \), and the power transferred to electrons changes with distance along the jet according to \( L_e(z) \propto z^{-2} \) (model A); (2) \( \alpha = 2.6 \) and \( L_e(z) \propto z^{-2} \) (model B), (3) \( \alpha = 2.6 \) and \( L_e(z) = \text{const} \) (model C). The cut-off in the electron spectrum is determined by \( \xi = 0.1, \eta = 0.1 \). The upper and bottom panels show the spectra produced in the jet and the jet + counter-jet, respectively. The \( \gamma \)-ray spectra above are shown for the minimum flux above 100 GeV, i.e. at the phase 0, counted from the location of the compact object behind the massive star (full curves), and for the maximum flux at the phase \( \sim 0.45 \) and 0.55 (dashed curves). The synchrotron spectrum produced by electrons in the jet are shown by the full curves below MeV energies. The spectrum from Cyg X-1 reported by the COMPTEL telescope and the upper limit obtained based on the EGRET data (McConnell et al. 2000, 2002) are shown by thin full curves and marked by C and E, respectively. The sensitivities of the MAGIC and VERITAS telescopes are shown by double dot-dashed and dotted curves and marked by M and V, respectively (see e.g. Lorenz 2000).

However, in the context of the recent discoveries of the TeV emission from massive binary systems (i.e. LS 5039 and LS I +61 303), which have similar orbital parameters to Cyg X-1 (i.e., a massive star and separation of the components), it is reasonable to predict the level and spectral features of the possible high energy \( \gamma \)-ray emission also from this object. Based on the IC \( e^\pm \) pair cascade model (Bednarek 2006b), considered here for Cyg X-1, we were able to predict the phase dependent TeV emission from LS I +61 303 (Albert et al. 2006). In the case of Cyg X-1, we normalize the cascade \( \gamma \)-ray spectra expected from this object to the upper limit derived from the EGRET data. Note that, the MeV \( \gamma \)-ray emission from Cyg X-1 is \( \sim 1\% \) of its total bolometric power (McConnell et al. 2002), and the EGRET upper limit in the GeV energies is again on the level of 10% of the MeV emission. On the other hand, in the cascade model which we consider almost all energy from relativistic electrons in the jet is transferred to gamma-rays (and also secondary pairs), see Bednarek (2006b). Since the jet power is expected to be comparable to the observed luminosity of the Cyg X-1, we conclude that the considered model is consistent if only a small part of jet energy is converted into relativistic electrons (i.e. \( \sim 0.1\% \)). The applied normalization to the EGRET upper limit allows us to estimate the level of the TeV \( \gamma \)-ray flux and spectrum from Cyg X-1. In Figs. 6 we show the comparison of the results of calculations with the observational constraints at lower energies. The upper and the lower panels we show the cascade \( \gamma \)-ray spectra escaping toward the observer located at the inclination angle \( i = 30^\circ \) for the case of their production in the jet and the jet+counter-jet (the sum of both), respectively. Since we have no detailed information about the spectral shape in the GeV energy range from the EGRET observations (but only the upper limit), electrons injected into the jet with different spectra and injection efficiencies along the jet have to be considered. At first we consider the model with very flat electron spectrum (differential spectral index equal to -2) and the power transferred to electrons which changes with distance along the jet according to \( L_e(z) \propto z^{-2} \) (model A). In fact, such flat electron spectrum seems to be not very realistic if we compare the spectral features of the source LS I +61 303 (the object of our previous modeling) and the spectrum of Cyg X-
1. The electron spectrum with the index 2 postulates the appearance of a completely new component in the high energy spectrum of Cyg X-1 which does not lay on the extrapolation from the MeV energy range. The comparison of the calculated cascade spectra with the available data and the sensitivities of the present MAGIC telescope (M) and the future VERITAS telescope (V) is shown in Fig. 6a, b. The dashed and full curves show the expected spectra when the compact object is in front of and behind the massive star HDE 226868. Clearly, for such model parameters, Cyg X-1 can be potentially detected at energies above ~100 GeV by the MAGIC telescope and above a few 100 GeV by the VERITAS telescope when the compact object is in front of the massive star. We also show the synchrotron spectrum which is produced by electrons accelerated in the jets assuming that the Doppler boosting is not important (bumps at lower energies marked by full curves). These spectra are at a much lower level than the observations of Cyg X-1 in the MeV energy range and cannot be responsible for this emission. Note, however, that if significant Doppler boosting is discovered in Cyg X-1 (the speed of the jet comparable to the velocity of light), the flux in the calculated synchrotron spectrum should go up with respect to the $\gamma$-ray spectra. This is due to the fact that the cascade $\gamma$-ray spectra are mainly formed outside the jet, i.e. inside the whole volume of the binary system where the plasma move with the wind velocity of the massive star. In such a case, the Doppler boosting can be only important for the synchrotron radiation but is clearly unimportant for cascade $\gamma$-rays. This MeV $\gamma$-ray emission can also originate in another scenario, e.g. in the hot corona of the accretion disk (e.g. Zdziarski & Gierliński 2004, Chakrabarti & Mandal 2006) or in the inner part of the jet close to its base (a scenario not considered in this paper) as a result of Comptonization of the disk radiation and possible IC cascading in the disk radiation, e.g. Aharonian et al. 1985, Coppi, Blandford & Rees 1993).

The calculations with the more realistic model parameters (see Table 2) are compared with the Cyg X-1 data and sensitivities of the Cherenkov telescopes and are shown in Figs. 6. We show in Figs. 6a the $\gamma$-ray spectra from the jet and in Figs. 6b the jet + counter-jet, which are calculated for electrons with the differential spectral index $\propto E^{-2.6}$, and the power in electrons dropping along the jet according to $L_\gamma(z) \propto z^{-2}$ (model B). For these parameters, there is no chance for detection of TeV $\gamma$-ray emission neither by the MAGIC telescope above ~100 GeV nor by the Veritas telescope at ~1 TeV. Finally in Figs. 6c, f, the $\gamma$-ray spectra are shown for electrons injected with the steep spectrum ($\propto E^{-2.6}$) but with flat profile for the power transferred from the acceleration mechanism to electrons, $L_\gamma(z) = const$ (model C). For this model, a large power is transferred to electrons at larger distances from the base of the jet where the acceleration of electrons is saturated at larger energies. Then, the cascade $\gamma$-ray spectra at TeV energies are relatively flat, in spite of the strong $\gamma$-ray absorption effects. The $\gamma$-ray spectra produced from the jet, after normalization to the EGRET upper limit in the GeV energy range, have chance to be detected by the VERITAS telescope at TeV energies but not by the MAGIC telescope above ~100 GeV (Figure 6e). Note that the unboosted synchrotron spectra calculated in model B and C are at the lower level than in the model A due to different normalization in the GeV energy range.

### 6. Conclusions

We constrain the parameters of the IC $e^\pm$ pair cascade model for which we predict observable $\gamma$-ray fluxes from Cyg X-1 at energies >100 GeV by the MAGIC and/or VERITAS telescopes. The main conclusions from the analysis of this model for the $\gamma$-ray production in microquasars are reported in the following.

The detection of the TeV $\gamma$-ray emission from Cyg X-1 by Cherenkov telescopes can occur only under very special conditions for the acceleration of electrons in the jet as described in the model herein considered, and for an acceleration efficiency parameter $\xi$, the magnetic field strength parameter $\eta$, a flat spectrum of electrons, and a flat profile of the conversion of energy from the acceleration mechanism to electrons along the jet. These conditions are not very likely and do not fit nicely to $\gamma$-ray observations of Cyg X-1 at the MeV-GeV energy range.

Provided that such strict conditions for the acceleration of electrons are met (e.g. as in the considered model A), we have found that in the case of compact massive binary systems with circular orbits of the Cyg X-1 type, the highest chances for detection of TeV $\gamma$-ray emission by the Cherenkov telescopes are for phases $\sim 0.45$ and $\sim 0.55$, counted from the position of the compact object behind the massive star. The flux expected at the moment when the compact object is exactly in front of the massive star is a factor of $\sim 2$ lower. The GeV and TeV $\gamma$-ray fluxes should be anticorrelated. The largest GeV flux is expected when the compact object is behind the massive star. The GeV $\gamma$-ray flux should vary by a factor of $\sim 5$ and the TeV flux by a factor of $\sim 20$ with the orbital period of Cyg X-1/HDE226868 system.

We want to remind that the above conclusions concerning possible detection of the very high energy $\gamma$-ray emission from Cyg X-1 are based on the assumption that the upper limit derived from the EGRET observations provides correct constraints on the multifrequency spectrum of Cyg X-1, independent of the activity state of this binary system. In fact, this upper limit is consistent with

### Table 2. Parameters of the models considered in Fig. 6

| Model | A | B | C |
|-------|---|---|---|
| differential spectrum of electrons: $N(E) \propto E^{-2}$ | $E^{-2.6}$ | $E^{-2.6}$ |
| injection number of electrons along the jet: $L_\gamma(z) \propto z^{-2}$ | $z^{-2}$ | $const.$ |
the extrapolation of the γ-ray spectrum reported by the COMPTEL telescope from the Cyg X-1 region during the hard X-ray state of this source. Such flat MeV spectrum is not observed from Cyg X-1 during its other activity states (e.g. McConnell et al. 2000, 2002).

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