Gravitational lens time-delay as a probe of a possible time variation of the fine-structure constant

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Received: 3 April 2021 / Accepted: 5 June 2021 / Published online: 22 June 2021
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Abstract A new method based on large scale structure observations is proposed to probe a possible temporal variation of the fine-structure constant ($\alpha$). Our analyses are based on time-delay of Strong Gravitational Lensing and Type Ia Supernovae observations. By considering the runaway dilution scenario, where the cosmological temporal evolution of the fine-structure constant is given by $-n\ln(1+z)$, we obtain limits on the physical properties parameter of the model ($\gamma$) at the level $10^{-2}$ ($1\sigma$). Although our limits are less restrictive than those obtained by quasar spectroscopy, the approach presented here provides new bounds on the possibility of $\Delta\alpha/\alpha \neq 0$ at a different range of redshifts.

1 Introduction

It is well-known that the standard physics is characterized by a set of laws and fundamental couplings which were historically assumed to be space-time invariant. One of the first contributors to ask about this conjecture was Dirac [1], arguing that fundamental couplings might not be pure numbers that occur in many theories, but they might depend on the state of the Universe. Thereafter, many theoretical and observational approaches have come searching for a space-time variation of the fundamental couplings of nature (see a detailed review in [2,3]). Although the search for a possible varying fundamental couplings has raised the interest of many cosmologists, the general relativity theory prohibits any variation since it is the fine structure constant, and $c$ the speed of the light.

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predict strong variations in the very early universe. There are other probes using distinct astrophysical observable, such as black hole in a high gravitational potential [28], galaxy cluster [29], Big-Bang Nucleosynthesis [30], among others [31,32]. Nonetheless, in the Ref. [33] it was revisited the so called $\Lambda(\alpha)$CDM framework where the cosmological constant is $\Lambda \propto \alpha^{-6}$. By using cosmological observations as SNe Ia, BAO and CMB along with 313 data from absorption systems in the spectra of distant quasars, constraints on two specific $\Lambda(\alpha)$CDM models were performed. The authors found $\Delta \alpha / \alpha \approx 10^{-6}$, very similar to the results discussed by [34]. On the other hand, variations in $\alpha$ have also been explored on the Earth with atomic clock measurements [35] and isotope ratio measurements [36], where its sensitivity (around $10^{-18}$) provides a useful constraint on a possible temporal variation of $\alpha$.

Among scenarios beyond standard model that produce a temporal variation of alpha, we can cite a particular class of string theory inspired-models, the so-called runaway dilaton model [37,38]. In this scenario, the runaway of the scalar field dilaton towards strong coupling may yield a temporal variation of the fine-structure constant. In this context, a possible evolution of $\alpha$ at low and intermediate redshifts is given by $\Delta \alpha / \alpha \approx -\frac{1}{3\nabla a} \dot{\phi}_0 \ln (1 + z) = -\gamma \ln (1 + z)$, where $\gamma \equiv \frac{1}{3\nabla a} \dot{\phi}_0, \dot{\phi}_0$ is the current value of the coupling between the dilaton and hadronic matter, and $\phi_0 = \frac{\phi_0}{a}$ at the present time.

In order to check a possible temporal variation of the fine-structure constant in runaway dilaton scenarios, some methods using astronomical data have been developed in recent years. By using galaxy clusters observations, for instance, the Ref. [39] proposed an approach by using gas mass fraction (GMF) measurements and luminosity distances of type Ia supernovae (SNe Ia) to put constraints on $\Delta \alpha / \alpha$. The GMF measurements used in the analyses were obtained via the Sunyaev–Zeldovich (SZ) effect at 148 GHz by the Atacama Cosmology Telescope, and the SNe Ia data from the Union2.1 compilation. The results showed no strong evidence for $\Delta \alpha / \alpha \neq 0$. More recently, the Ref. [40] argued that the galaxy cluster scaling-relation $Y_{\text{SZ}} D_A^2 / C_{\text{SZ}} Y_X$ can also be used to put constraints on the runaway dilaton model. The authors found that $Y_{\text{SZ}} D_A^2 / C_{\text{SZ}} Y_X \propto \alpha^3$ by considering a direct relation between a temporal variation of the fine-structure constant and a possible deviation of the cosmic distance duality relation (see also [41]). Once again, the results showed no strong evidence for $\Delta \alpha / \alpha \neq 0$. Several other tests capable of probing such temporal variation of $\alpha$ with galaxy cluster observations have been emerging since then (see e.g. [42–44] and references therein).

In this paper, we present a new method based on time-delay of strong gravitational lensing (SGL) systems and type Ia of supernovae observations to obtain limits on a possible temporal variation of the fine-structure constant in runaway dilaton scenario. The samples used to perform our approach are: 19 two-image time-delay lensing systems compiled by the Refs. [45,46] jointly with 1048 spectroscopically confirmed SNe Ia compiled by [47]. Moreover, we consider a specific catalog containing 158 confirmed sources of strong gravitational lensing systems from the Ref. [48]. We obtain limits on the physical properties parameter of the runaway dilaton model ($\nu$) at the level $10^{-2}$ ($1\sigma$) in full agreement with recent limits by using galaxy clusters observations plus SNe Ia observations.

The work is organized as follows: in Sect. 2 we develop our methodology. The theoretical framework is discussed in Sect. 3. In Sect. 4 we present the data set used to perform the analyses. In Sect. 5 the corresponding statistical analyses and discussions, and in Sect. 6 we finished with the conclusions.

### 2 Methodology

#### 2.1 Strong gravitational lensing systems

Strong gravitational lensing systems (SGL) can be used to investigate gravitational and cosmological theories and fundamental physics. Particularly, observed SGL systems and detected by SLACS, LSD, SLS2, and BELLS surveys have been largely used to fit observational bounds on different cosmological parameters. An useful quantity in this context should be Einstein ring ($\theta_E$). Under the assumption of the singular isothermal sphere (SIS) model to describe lens mass distribution, the Einstein radius $\theta_E$ is given by [49–51]:

$$\theta_E = \frac{4\pi \sigma^2_{\text{SIS}} D_{A_s} \theta_{E_s}}{c^2}, \quad (1)$$

where $D_{A_s}$ is the angular diameter distance (ADD) from the lens ($l$) to the source ($s$), $D_A$ the ADD from the observer to the source,$c_s$ is the speed of light between source and observer, and $\sigma_{SIS}$ is the velocity dispersion via SIS model. From Eq. (1) the multiple-image separation of the source depends only on the lens and source angular diameter distances. Nonetheless, the quantity of interest is

$$D \equiv \frac{D_{A_s}}{D_A} = \frac{\theta_E c_s}{4\pi \sigma^2_{\text{SIS}}}, \quad (2)$$
which can be written in terms of the fine-structure constant \( \alpha_s \equiv e^2 / \hbar c_s \) by:

\[
D = \frac{\theta_E e^4}{4\pi \alpha^2 \hbar^2 \sigma^2_{SIS}}. \tag{3}
\]

In order to obtain \( D \) from SGL systems observations one needs to make an assumption on the variation of alpha. Currently available data make the assumption \( \alpha_s = \alpha_0 \), the local value of the fine structure constant. \(^4\)

2.2 Time-delay systems

Time-Delay is another important observational consequence of Strong Gravitational Lensing and it can also be used as a powerful astrophysical tool. Based on the fact that photons follow null geodesics and they are originated from a distant source with distinct optical paths, they shall pass through dissimilar gravitational potentials \([49, 54, 55]\). Thus, the time-delay is caused by the difference in length of the optical paths and by the gravitational temporal variation originated in the passage through the effective gravitational potential of the lens.

Time-delay gives a correlation among the angular diameter distances from observer to lens \((D_{A_1})\), from observer to source \((D_{A_0})\), and from lens to source \((D_{A_{ls}})\) by \([56]\):

\[
\Delta \tau = \frac{1 + z_l}{c_s} \frac{D_{A_1} D_{A_0}}{D_{A_{ls}}} \left[ \frac{1}{2} (\beta - \bar{\beta})^2 - \Psi(\bar{\theta}) \right], \tag{4}
\]

where \( \Delta \tau \) is the so-called time-delay, \( \beta \) and \( \bar{\beta} \) are, respectively, the angular positions of the image and the source, \( z_l \) the lens redshift, and \( \Psi \) is the lens effective gravitational potential. Thereafter, for a two image lens system \((A \text{ and } B)\) with SIS mass profile describing the lens mass, we can obtain \([57]\):

\[
\Delta t = \Delta \tau (A) - \Delta \tau (B) = \frac{1 + z_l}{2c_s} \frac{D_{A_1} D_{A_0}}{D_{A_{ls}}} \left[ \theta_A^2 - \theta_B^2 \right]. \tag{5}
\]

Defining the quantity \( \frac{D_{A_1} D_{A_0}}{D_{A_{ls}}} \) as time-delay angular diameter distance \( D_{A_{\Delta t}} \):

\[
D_{A_{\Delta t}} = \frac{D_{A_1} D_{A_0}}{D_{A_{ls}}} = \frac{2c_s \Delta t}{(1 + z_l)(\theta_A^2 - \theta_B^2)}. \tag{6}
\]

which can be rewritten in terms of \( \alpha_s \) by:

\[
D_{A_{\Delta t}} = \frac{2e^2 \Delta t}{\hbar \alpha_s(1 + z_l)(\theta_A^2 - \theta_B^2)}. \tag{7}
\]

Also in this case one needs to make an assumption on the variation of alpha to obtain \( D_{A_{\Delta t}} \) from the measurements of time delay, and currently available data set \( \alpha_s = \alpha_0 \).

3 Theoretical framework

3.1 Scalar–tensor theory of gravity

Theories of modified gravity associated to a scalar field with a non-minimal multiplicative coupling to the usual electromagnetic Lagrangian lead to violations of the Einstein Equivalence Principle (EEP) in the electromagnetic sector. The matter Lagrangian of this type of theories is given by \([53, 58]\)

\[
S_{\text{mat}} = \sum_i \int d^4x \sqrt{-g} h_i(\phi) L_i(g_{\mu\nu}, \Psi_i), \tag{8}
\]

where \( h_i(\phi) \) is a function of the scalar field \( \phi \), and \( L_i \) are the Lagrangians for the different matter fields. In this context, the fine-structure constant and the cosmic distance duality relation (CDDR) change with cosmological time, and both are intimately and unequivocally related to each other by \([53, 58]\):

\[
\frac{\Delta \alpha}{\alpha}(z) = \frac{h(\phi_0)}{h(\phi)} - 1 = \eta^2(z) - 1, \tag{9}
\]

where \( \eta \) takes into account any deviations of the CDDR. Considering \( \alpha = \alpha_0 \phi(z) \), where \( \alpha_0 \) is the current value of \( \alpha \), the Eq. (9) gives \( \eta^2(z) = \phi(z) \) \([53]\). Therefore, the Eqs. (3) and (7) shall be rewritten, respectively, by

\[
D = D_0 \phi^{-2}(z_s) \tag{10}
\]

and

\[
D_{A_{\Delta t}} = D_{A_{\Delta t,0}} \phi^{-1}(z_s), \tag{11}
\]

where, \( D_0 \equiv \frac{e^2 \theta_E}{4\pi \alpha_0 \sigma^2_{SIS}} \) and \( D_{A_{\Delta t,0}} \equiv \frac{2e^2 \Delta t}{h_{\alpha_0}(1 + z_l)(\theta_A^2 - \theta_B^2)} \). It is important to clarify that the subscript 0 denotes the current quantities that have been obtained in literature by assuming \( \alpha_s = \alpha_0 \). It does not mean local values of \( D \) or \( D_{A_{\Delta t}} \). The \( D \) or \( D_{A_{\Delta t}} \) quantities (Eqs. (10), (11)) are the true observational values if one corrects a possible \( \alpha \) variation.

By considering the definitions \( D \equiv D_{A_{\Delta t}} / D_{A_1} \) and \( D_{A_{\Delta t}} = D_{A_{\Delta t,0}} / D_{A_{\Delta t,0}} \) jointly with the Eq. (10) and (11), it is possible to
obtain:
\[
D_{A_l} = D_0 D_{A_{\alpha,0}} \phi^3(z_s) \\
\Rightarrow \phi^3(z_s) = \frac{D_0 D_{A_{\alpha,0}}}{D_{A_l}}.
\]  
(12)

Finally, to perform our tests and impose new limits on a possible time-variation of \( \alpha \), it is necessary to know \( D_{A_l} \) for each SGL. This quantity can be obtained by SNe Ia luminosity distance measurements with identical redshifts from those of the SGL system sample. Since the SNe Ia observations also can are affected by a varying \( \alpha \), we shall consider a deformed CDDR as \( D_{A_l} = \eta^{-1}(z_l)(1 + z_l)^{-2} D_{L_l} \) [59, 60] and the fact that \( \eta^2(z) = \phi(z) \) [53]. Then, one may obtain:
\[
\frac{\phi^{1/2}(z_l)}{\phi^3(z_s)} = \frac{D_{L_l}}{D_0 D_{A_{\alpha,0}}(1 + z_l)^2}.
\]  
(13)

This is our key equation, if \( \alpha = \alpha_0 \) the right side is equal to unity and no time variation of \( \alpha \) is possible. It is possible to use this expression to impose new limits on a possible time-variation of \( \alpha \) in the context of a very specific string-inspired model, the so-called runaway dilaton Model.

3.2 Runaway Dilaton model

In this paper, we focus on the runaway dilaton model [37, 38]. The main idea behind such model is exploiting the string-loop modification of the four dimensional effective low-energy action, where its Lagrangian is given by:
\[
\mathcal{L} = \frac{R}{16\pi G} - \frac{1}{8\pi G} (\nabla \phi)^2 - \frac{1}{4} B_F(\phi) F^2 + \ldots,
\]  
(14)

where \( R \) is the Ricci scalar, and \( B_F(\phi) \) is the gauge coupling function. The Runaway Dilaton model is a particular case of scalar–tensor theories of gravity commented in Sect. 3 [37, 38, 53]. One can show that the Friedmann equation in this scenario is as follows
\[
3H^2 = 8\pi G \sum_i \rho_i + H^2 \phi^2,
\]  
(15)

where the sum is over the components of the universe, and \( H \) is the Hubble parameter. The relevant parameter of this model is the coupling of \( \phi \) to hadronic matter. Nevertheless, the runaway of the dilaton towards strong coupling can lead to temporal variations of \( \alpha \), and its variation at low and intermediate redshifts is given by [3]
\[
\frac{\Delta \alpha}{\alpha} \approx -\frac{1}{40} \beta_{\text{had},0} \phi(1 + z),
\]  
(16)

where \( \beta_{\text{had},0} \) is the current value of the coupling between the dilaton and hadronic matter, and \( \phi(1 + z) \).  

4 Reconstruction method and data

4.1 Gaussian processes

In order to obtain a continuous regression of the luminosity distance and \( D_0 \) in function of \( z \), we apply the Gaussian Processes (GP) method to the data sets described in Sects. 4.2 and 4.4. The GP reconstruction is performed by choosing a prior mean function and a covariance function which quantifies the correlation between the values of the dependent variable of the reconstruction and is characterized by a set of hyperparameters. In our reconstructions of \( D_0 \) and \( D_L \), we choose zero as the prior mean function to avoid biased results and a Gaussian kernel as covariance function given by:
\[
k(z, z') = \sigma^2 \exp \left(-\frac{(z - z')^2}{2l^2}\right),
\]  
(17)

where \( \sigma \) and \( l \) are hyperparameters related to the variation of the estimated function and its smoothing scale, respectively. To optimize the hyperparameter values, we maximize the logarithm of the marginal likelihood:
\[
\ln \mathcal{L} = -\frac{1}{2} y^T [k(x, x) + C] y - \frac{1}{2} \ln |k(x, x) + C|,
\]  
(18)

where \( x \) and \( y \) are the vectors of the independent and dependent data variables, respectively, and \( C \) is the covariance matrix of the data (error matrix). We use the code GaPP\(^6\) to perform the GP reconstruction of the \( D_L \) and \( D_0 \) data (see Ref. [61] for more details about GP).

4.2 Supernova type Ia

The samples of luminosity distance to the lens is obtained from the Pantheon catalog [47]. This is the most recent wide and refined sample of SNe Ia measurements composed by 1048 spectroscopically confirmed SNe Ia and covers a redshift range of \( 0.01 \leq z \leq 2.3 \). We must obtain the SNe Ia at the same redshift to the lens, for this purpose we apply the GP method to find out the central value with the corresponding variance. The first \( D_L \) sample is constructed from the apparent magnitude \( \langle m_h \rangle \) Pantheon catalog considering the absolute magnitude \( \langle m_h \rangle = -19.23 \pm 0.04 \) (henceforth R19) via the relation:
\[
D_L = 10^{\langle m_h \rangle - M_b - 25)^{1/5}} \text{Mpc}.
\]  
(19)

\(^5\) This expression assumes that the prior mean function is equal to 0 and we omit the term that depends on the number of data points.

\(^6\) https://github.com/carlosandrepaes/GaPP.
4.3 Time-delay

We use a data set of 12 two-image time-delay lensing systems compiled by [45]. The use of two-image lensing systems is justified by the consistency with SIS mass profile and its simplicity. However, this selection criterion is necessary but not sufficient to guarantee a SIS mass profile for the lens. Thus, as mentioned in Ref. [64], we include an additional error source denoted by $\xi$ which takes into consideration possible scatters of individual lenses from a pure SIS mass profile. Moreover, according to Ref. [65] $\xi$ can contribute up to 20% in the $D_{\Delta t}$ estimation. Adding $\xi$ quadratically the associated error we obtain

$$
\sigma_{D_{\Delta t},0}^2 = D_{\Delta t,0}^2 \left\{ \left( \frac{\sigma_{D_{\Delta t}}}{D_{\Delta t}} \right)^2 + 4 \left[ \frac{\sigma_{\theta_A} \theta_A}{\theta_B - \theta_A} \right]^2 \right\} + 4 \left[ \frac{\sigma_{\theta_B} \theta_B - \theta_A}{\theta_B - \theta_A} \right]^2 + \xi^2 \right\},
$$

(20)

where $\sigma_{\theta_A}$ and $\sigma_{\theta_B}$ are the errors associated with the source images positions A and B, respectively, and $\sigma_{D_{\Delta t}}$ the time-delay error. In addition, we consider seven more time-delay systems obtained by the COSMOGRAIL’s Wellspring (H0LiCOW) collaboration and listed in Table 2 of [46]. Each system were modeled using constraints from high-resolution HST and/or ground-based AO (Adaptive Optics) imaging data (see more details in [66]). Since the data from the Ref. [46] present asymmetric error bars, the data were treated using the method from the Ref. [67,68] (see Fig. 2).

4.4 Einstein radius

We consider a specific catalog containing 158 confirmed sources of strong gravitational lensing presented in Ref. [48]. This compilation includes 118 SGL systems identical to the compilation in Ref. [49] along with 40 new systems recently discovered by SLACS and pre-selected by [69] (see Table I in Ref. [48]).

However, studies using SGL systems have shown that the pure SIS model may not be an accurate representation of the lens mass distribution when $\sigma_0 < 250$ km/s, for which non-physical values of the quantity $D_0$ are usually obtained ($D_0 > 1$). In addition, in Ref. [48] it is mentioned the need for caution when using the SIS model as a reference model, since the impact caused on the density profile can lead to deviations in the observed stellar velocity dispersion ($\sigma_0$). It was also observed the need of introducing an additional intrinsic error of approximately 12.22% in order to obtain a better concordance between the data and the $\omega$CDM and $\Lambda$CDM models (see [48] for more details).

Thus, we will consider a general approach to describe the mass distribution of lens-type galaxies, the one in favor of the $Y$ power-law index model (PLAW), where $\rho \propto r^{-Y}$. This type of model is important due to several recent studies have shown that the loops of the density profiles of individual galaxies have exhibited a non-negligible spread of the SIS model [70]. Thus, the term $D_0$ of equation (10) is written by:
5 Analysis and discussion

We use Markov Chain Monte Carlo (MCMC) methods to calculate the posterior probability distribution functions (pdf) of the free parameter ($\Theta = \gamma$) [73]. Thus, the likelihood distribution function is given by:

$$L(Data | \Theta) = \prod_i \frac{1}{\sqrt{2\pi} \sigma_{\mu}} exp \left( -\frac{1}{2} \chi^2 \right),$$

where

$$\chi^2 = \sum_i \frac{\left[ W_i - \frac{\phi^{1/2}(z_i)}{\phi^{1/2}(z_{s})} \right]^2}{\sigma_{\mu}^2},$$

$$W_i \equiv \frac{D_{L,i}}{D_{0,i} D_{A_{\Delta \theta,0}} (1 + z_i)^2},$$

and

$$\sigma_{\mu}^2 = \sigma_{W_i}^2 + \sigma_{D_{L,i}}^2 + \sigma_{D_{A_{\Delta \theta,0}}}^2.$$
\(D_0\) at the redshift of each time-delay system. Then, we use the reconstruction of \(D_0\) obtained with GP method (see Sect. 4.4). Moreover, in order to obtain a \(\chi^2_{\text{red}} \approx 1\) (see Eq. 24) in our analyses, it was added an additional intrinsic error (\(\sigma_{\text{int}}\)). We estimate it to be \(\approx 33\%\) for [45] and \(\approx 23\%\) for [46]. For both samples together, \(\sigma_{\text{int}}\) was estimated to be \(\approx 30\%\). The addition of intrinsic error is necessary due to some possible reasons: i) the reported errors are possibly underestimated, and (ii) that there is an additional unrecognized systematic effect that has yet to be included in the analysis as, for instance, possible random deviations from power law model. This kind of approach has been used in previous analyses with SGL systems (see [48, 65]).

Our results are as follows (in 1 \(\sigma\) c.l.):

- By considering \(D_L\) measurements from the Pantheon compilation with \(M_b = -19.23 \pm 0.04\), we obtain:
  \[\gamma = -0.03^{+0.05}_{-0.06}\text{ for the 12 time-delay systems [45], and}\]
  \[-0.17^{+0.07}_{-0.06}\text{ for the 6 time-delay systems [46]. For both samples together:}\]
  \[\gamma = -0.09^{+0.04}_{-0.05}\text{ (see Table 1).}\]

- By considering the \(D_L\) measurements from Pantheon compilation with \(M_b = -19.43 \pm 0.02\), we obtain:
  \[\gamma = +0.06^{+0.04}_{-0.05}\text{ for the systems in Ref. [45], and}\]
  \[-0.13^{+0.05}_{-0.06}\text{ considering the systems in Ref. [46].}\]
  For both samples together we obtain \(\gamma = -0.06^{+0.04}_{-0.05}\) (see Table 1).

We also performed our analyses with smoothing technique [74–76] on \(D_0\) quantity, the results are in full agreement with those by using Gaussian Process.

6 Conclusions

The search for a possible time-space variation of the fundamental constants of nature has raised the interest of many cosmologists due to its possibility of revealing a new underlying physics. In this context, we provided a new method capable of probing a possible temporal evolution of the fine-structure constant by considering time-delay of Strong Gravitational Lensing Systems. A possible temporal variation of \(\alpha (\alpha = \Delta \alpha/\alpha)\) was investigated in a class of runaway dilaton models, where \(\phi(z) = 1 - \gamma \ln(1 + z)\), where \(\gamma\) is a free parameter.

The most restrictive bounds come from the joint analysis using the two samples of time-delay systems together from the Refs. [45, 46]. We obtained \(\gamma = -0.09^{+0.04}_{-0.05}\) and \(\gamma = -0.06^{+0.04}_{-0.05}\) for \(D_L\) measurements from Pantheon+R19 and Pantheon+P18, respectively (see Fig. 4, Table 1).

Finally, it is important to stress that recently the authors in the Ref. [22] showed that fitting turbulent models in quasars necessarily generates or enhances model non-uniqueness, adding a substantial additional random uncertainty to \(\Delta \alpha/\alpha\) obtained from quasar absorption systems. Basically, any given absorption system can be fitted equally well by many slightly different models, each furnishing a different value to \(\Delta \alpha/\alpha\). Therefore, although SGL plus time-delay systems are not as much competitive as the limits imposed by quasar absorption systems, the constraints imposed in this paper provide new and independent limits on a possible temporal variation of the fine-structure constant.

Acknowledgements The authors thank to Brazilian scientific and financial support federal agencies, CAPES, and CNPq. RFLH thanks to CNPq No.428755/2018-6 and 305930/2017-6.

Data Availability Statement This manuscript has no associated data or the data will not be deposited. [Authors’ comment: The data can be easily found in literature.]

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Funded by SCOAP3.

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