Dynamic on-bottom stability analysis of subsea pipelines using finite element model-based general offshore analysis software: a case study

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Abstract

Background: The dynamic on-bottom stability analysis represents a fundamental task in the design process of the subsea pipelines. Such analysis ensures the stability of the as-laid pipeline on the seabed against the lateral displacements, which are induced by the surrounding hydrodynamic forces. In this paper, the dynamic on-bottom stability analysis of a subsea pipeline is performed using finite element-based advanced offshore engineering simulation software called Flexcom. The latter predicts the pipeline response in a time-domain simulation based on a given environmental condition (i.e., the sea state, the soil frictional resistance, and the nonlinear behavior of the pipeline). A case study is conducted on a 22-in.-diameter pipeline, which is placed on a sandy soil in shallow water, under different loading combinations from two-dimensional irregular waves and a steady current.

Results: The resultant maximum lateral displacements and the associated stresses decreased by increasing the concrete weight coating thickness. Pipeline response due to drag, lift, and inertia forces increased by increasing the total water particle velocity induced from the summation of wave-induced particle velocity and current velocity. Different random wave patterns generated from different random seed numbers assigned to wave components are important to verify the selection of the concrete weight coating thickness. Ignoring passive soil resistance reduced the total soil resistance significantly and resulted in conservative stability weight requirement.

Conclusions: Several factors influence the pipeline stability such as pipeline submerged weight, hydrodynamic loads induced by random sea states, and soil friction model being used. The dynamic on-bottom stability analysis can optimize the design and results in less concrete weight coating if the actual case is modeled accurately; therefore, ignoring passive soil resistance reduced the prime advantage of this analysis compared to other simplified methods.

Keywords: Dynamic on-bottom stability, Pipe–soil interaction, Subsea pipelines, Finite element analysis (FEA), Hydrodynamic loads, Time-domain simulation

1 Background
 Various design methods may be employed for on-bottom stability assessment of the subsea pipelines on the basis of hydrodynamic loads and soil resistance. These methods may be split into three categories as follows [49]. The first category includes the static analysis methods which are based on the force-balance calculation that is firstly introduced in DNV 1976 [15] and in which the...
pipeline movement is not allowed under the extreme sea state; these methods include Level 1 program of Pipeline Research Council International (PRCI) of the American Gas Association (AGA) and absolute lateral static stability (ALSS) method presented in RP-F109 [16]. The second category includes the empirical or calibrated design methods such as the Level 2 program of the PRCI of the AGA [18, 33] which is known as AGA Level 2, and the generalized lateral stability (GLS) method presented in RP-F109 [16, 17, 25]. The third category includes the dynamic lateral stability (DLS) analysis, which is based on the time-domain simulation of the pipeline dynamic response, the sea state-induced hydrodynamic loads, and the pipe–soil interaction, using specialized finite element (FE) software packages. The DLS analysis usually represents the basis for validating other calibrated methods, to ensure stability and to provide lower-conservative and higher-optimized design.

The DLS analysis method is not widely used because of the associated complexities than other conventional stability methods that are represented by building a model with accurate simulation involving the fluid–pipe–soil interaction, the limited availability of the software packages, and the incentive to replace the static and calibrated methods with advanced dynamic ones is not existing. In this regard, there are only two software packages recognized in the industry for the dynamic on-bottom stability analysis of the subsea pipelines: PONDUS [21] and AGA Level 3 [1, 26, 33]. It is possible to use the other general FE software packages such as ABAQUS [12] and ANSYS [4] with integrated modules for modeling the hydrodynamic loads and the pipe–soil interaction. Ose et al. [31] introduced the first finite element model using ABAQUS [20] for the dynamic on-bottom stability analysis of the pipelines by using simplified modeling of the hydrodynamic loads and the mutual pipe–soil interaction. Bai and Yu [8] used ABAQUS to compare the on-bottom stability analysis results from the finite element model versus RP-E305 [13] to ensure the validity of the numerical model. ABAQUS has also been used to build and solve the numerical model of pipeline stability problems using a finite element method as presented in Yang and Wang [47] and Bai et al. [7]. Based on different methodologies of calculating the hydrodynamic loads and the pipe–soil interaction, other modules have been developed and integrated with the ABAQUS FE solver for dynamic on-bottom stability analysis of the pipelines. These modules are referred to by different names, such as SIMSTAB [50], UWAIN'T [40], and CORUS-3D [6]. SIMSTAB has been utilized in several case studies as presented in Ref. [3, 24, 34]. UWAIN’T has been developed based on several numerical models developed by Tian and Cassidy [37–39]. CORUS-3D has been used to study the dynamic response of pipelines as presented in Ref. [23, 28, 48].

Offshore software packages such as Flexcom [46] and OrcaFlex [30] may also be used as will be described in the subsequent sections of this paper by using Flexcom software [46].

In this paper, the DLS analysis is conducted on a 22-in.-diameter pipeline installed in shallow water on a sandy seabed. The sea state consists of irregular waves, represented by the Joint North Sea Wave Project (JONSWAP) spectrum [19], and a steady current. It is worth mentioning that this paper is devoted to studying the installation phase of the pipeline with an empty condition, as a worst case, under the following combined loads from waves and currents: 1-year return period values (RPV) wave + 10-year RPV current and 10-year RPV wave + 1-year RPV current.

The acceptance criteria of the on-bottom stability design of the pipelines depend on the design target and the factors that may affect the integrity of the pipeline. The acceptance criteria may be achieved either by the maximum allowable lateral displacement of the pipeline or by the stress limits for the design of the pipeline. Using both criteria, the numerical results are presented (sequentially) in the relevant subsections of this paper.

2 Methods

The dynamic on-bottom stability analysis of a subsea pipeline is performed by using finite element-based advanced simulation software, which is named Flexcom [46]. Flexcom is a highly versatile software package, which is commonly used in the structural analysis of conventional and unconventional offshore structures. The pipeline is modeled as a line with an automatic mesh generation, depending on the specified element length. The structural geometric properties (i.e., internal and external diameters, wall thickness, Young’s modulus, shear modulus, mass density, etc.) are assigned to the pipeline. The hydrodynamic loads in the form of drag, inertia, and lift force coefficients are allocated to the pipeline. The external and internal coatings, such as corrosion and concrete coatings, are added by deciding the thickness of each coating layer. The sea state consists of two-dimensional irregular waves accompanied by a steady current, and both are perpendicular to the pipeline.

Figure 1 shows the external forces (including the wave-induced hydrodynamic forces, the self-weight of the pipeline, and the soil resistance) which affect the subsea pipeline segment.

The time-domain simulation is performed for a duration of 3 h (10,800 s), as recommended in RP-F109 [16]. To perform full dynamic stability analysis for the pipeline, three different types of analyses are performed and
then subsequently aggregated into one dynamic analysis. These three types of analyses include static analysis, quasi-static analysis, and time-domain dynamic analysis.

The static analysis is performed to study the effect of the time-independent loadings such as water current and temperature loadings. In such analysis, the full model is designed to include the geometrical layout of the pipeline and its material and hydrodynamic properties, the environmental properties, as well as the geomechanical properties of the soil (shear strength, friction, adhesion, compressibility, abrasion, corrosion, permeability, seepage, lateral earth pressure, consolidation, bearing capacity, slope stability), and geotechnical properties of the soil (grain-size distribution, weight–volume relationships, relative density, Atterberg/consistency limits, soil texture, soil phases, etc.).

In the quasi-static analysis, all vertical constraints along the length of the pipeline are removed, and the pipeline is allowed to fall onto the seabed, under the combined effect of the gravity and buoyancy loads. Settling the pipeline quickly over the seabed under the combined effect of the gravity and buoyancy loads may be performed by specifying a significant mass damping to minimize initial transients. It is worth mentioning that the static and quasi-static analyses merely facilitate contact initiation between the pipeline and the seabed for penetration, due to the mutual action of pipeline self-weight and the seabed soil stiffness.

The dynamic analysis is performed in the time domain, to investigate the effect of the time-dependent loads (e.g., the wave loads, etc.), and the nonlinear response of the concrete-coated pipeline. For a given design condition, in which the pipeline is required to withstand combined static and dynamic loads, Flexcom [46] builds a fully dynamic solution for the combined loads by superposing the static, quasi-static, and dynamic analyses and then integrating all loads through all stages to get the full response of the pipeline at the end of the dynamic simulation.

### 2.1 Pipe–soil interaction

The interaction between the concrete-coated pipeline and the soil plays a significant role in the overall pipeline response and its contribution to the on-bottom stability as a resisting force to the surrounding hydrodynamic loads. Pipe–soil interaction is a very complex process because of the mutual influence between several parameters occurring throughout the pipeline installation and operation conditions. These parameters include the hydrodynamic cyclic loading on the pipeline and the pipe–soil interaction. Different hydrodynamic models have been developed based on the Morison’s equations [29] to accurately predict the cyclic loadings on the pipeline from waves and currents. These models were developed in Ref. [11, 17, 22, 25, 35, 36, 42].

The seabed soil resistance consists mainly of two components: the friction between the pipeline and the seabed soil (i.e., pure friction term) and the resistance due to the embedment of the pipeline into the seabed soil (i.e., passive resistance term). Lyons [27] experimentally concluded that the Coulomb friction model was not appropriate to describe the pipe–soil interaction, especially when the pipeline is placed on a soil of soft clay or loose
sand. Coulomb friction model does not function in the properties of wave, pipe, and soil.

The passive soil resistance models have initially been developed through the PIPESTAB project [10, 45] and then the AGA project [1, 9]. Both models were appropriate for use in predicting the dynamic pipeline response and for soft clay and loose sand soils, and both are implemented in PONDUS [21] and AGA software [33], respectively. By revisiting the PIPESTAB [10, 45] and AGA [1, 9] test data and other test data sources [32], an empirical approach was proposed by Verley and Sotberg [44] and Verley and Lund [43] to evaluate embedment for sand and clay soils, respectively. Both empirical approaches are considered the basis for the current design methodologies represented in RP-F109 [16].

Neglecting the passive soil resistance results in decreasing its total soil resistance (compared to its actual resistance); especially when the pipeline is placed on soil of soft clay or loose sand, the mutual interaction between the pipeline and the seabed soil may not be modeled accurately [49], and the pipeline may also largely displace in the lateral direction.

In the present case study, only the pure friction term is considered, due to the present capabilities of the software, and it is represented herein by the Coulomb friction model. The Coulomb friction model is considered as the simplest method for modeling the interaction between the pipeline and the seabed soil, and it can be used in both the static and dynamic analysis [49]. The Coulomb friction model assumes pure steady plastic frictional resistance between the pipeline and the seabed soil, and it does not consider any embedment-based cyclic loads or passive soil resistance.

To ensure the stability of the pipeline on the seabed in the presence of the Coulomb friction model, Eq. (1) must be satisfied.

\[ F_f \leq \mu F_c \]

where \( F_f \) is the friction force induced by the wave and current between the pipeline and the seabed in a direction parallel to the seabed, \( \mu \) is the coefficient of friction between the pipeline and the seabed, and \( F_c \) is the contact force induced by the wave and current between the pipeline and the seabed in a direction perpendicular to the seabed: \( F_c = W_s - F_L \), in which \( W_s \) is the pipeline submerged weight in a direction perpendicular to its span and \( F_L \) is the lift force induced by the wave and current in a direction perpendicular to the pipeline.

The seabed is modeled as an elastic flat surface having longitudinal and transverse friction coefficients and a constant linear stiffness value. For the concrete-coated pipelines (as per the present case study), the RP-F109 [16] recommends a friction coefficient (\( \mu \)) of 0.6 for sand and rock soil and 0.2 for clay soil.

At each iteration step of the time-domain simulation, the software surveys all the nodes of the structural model of the pipeline, to check whether they are in contact with the seabed or not (as long as either a rigid or elastic seabed has been specified as part of the model). If any node registered such contact, and if either or both of the seabed friction coefficients are nonzero, it is assumed as attached to the seabed (in the plane of the seabed) using a friction coefficient-based nonlinear spring approach.

In an ideal Coulomb friction model, each of these nonlinear springs would have a force–deflection relationship in which its stiffness (in the region corresponding to zero-deflection point) is infinite. Assume, momentarily, that such infinite force–deflection relationship refers to the longitudinal direction. If there is no longitudinal force on the node, the node does not move (corresponding to zero deflection in the infinite force–deflection relationship). Indeed, the node should remain in the same location until the total nodal force exceeds the limiting friction force (\( \mu F_c \)) at which point the node may move with this movement resisted by a constant force equal to the limiting friction force.

Flexcom [46] uses the modified Coulomb friction model as shown in Fig. 2, in which the infinite stiffness of the ideal Coulomb friction model (in the region corresponding to zero-deflection point) is replaced by a very high (but not infinite) stiffness (\( k \)) around the zero-deflection point. Such modification is performed by employing a slightly modified nonlinear spring characteristic.

The modified Coulomb friction model is performed to overcome the convergence difficulty inside the iterative scheme of the software while searching for the...
correct of the deflections (as in the case of most FE programs). This point is crucial to the operation of the seabed friction model. As the displacement at any arbitrary node depends, principally, on the stiffness of this section of the force–deflection curve, the stiffness is given by Eq. (2).

$$k = \frac{\mu F_c}{L_m}$$

(2)

where $k$ is the stiffness of the Coulomb friction model and $L_m$ is the mobilization length which is taken as 5% of steel pipeline outer diameter.

The value of the mobilization length ($L_m$) affects the stiffness of the nonlinear spring, i.e., the smaller is this value, the greater is the stiffness and the closer the friction model is to an ideal model. However, reducing the mobilization length of the pipeline makes it harder for the program to converge on a correct solution of the deflections. Note also that separate mobilization lengths may be used in both the longitudinal and transverse directions, with the longitudinal value typically being shorter than the transverse one.

2.2 Environmental loads

The environmental loads on the subsea pipelines, for an arbitrary-selected sea state, are represented by a combination of two-dimensional irregular waves and current loadings. Such loads are assumed to be dependent on the total velocity of water particles at the pipeline level and pipeline velocity. The total velocity of water particles is calculated as the summation of the wave-induced particle velocity and the steady current velocity. The wave-induced particle velocity is generated by the transformation of the wave spectrum at the sea surface. JONSWAP wave spectrum model [19] as given by Eq. (3) is selected to represent the two-dimensional irregular sea waves.

$$S_n(f) = \alpha \cdot g^2 \cdot (2\pi)^{-4} \cdot f^{-5} \cdot \exp\left[-\frac{2}{3}(f/f_p)^4\right] \cdot \exp\left[-\beta\left(\frac{f}{f_p}\right)^{4/\gamma}\right]$$

(3)

where $\alpha$ is the Phillip's constant, $g$ is the gravitational acceleration, $f$ is the computational wave frequency, $f_p$ is the spectral peak frequency, $f_p = T_p^2$, $\gamma$ is the peakedness parameter of the wave spectrum, and $\sigma$ is the spectral width parameter given by Equation (4).

$$\sigma = \begin{cases} 
0.07, & \text{if } f < f_p \\
0.09, & \text{else}
\end{cases}$$

(4)

Based on the value of $\psi = (T_p/\sqrt{\alpha})$, the value of Phillip's constant ($\alpha$) and peakedness parameter ($\gamma$) of the wave spectrum are calculated according to Eq. (5) and Eq. (6), respectively.

$$\alpha = \begin{cases} 
2.73H_c^2/T_p^4 & \psi \leq 3.6 \\
0.036 - 0.0056\psi & 3.6 < \psi < 5.0 \\
5.07H_c^2/T_p^4 & \psi \geq 5.0
\end{cases}$$

(5)

$$\gamma = \begin{cases} 
5.0 & \psi \leq 3.6 \\
e^{5.75-1.15\psi} & 3.6 < \psi < 5.0 \\
1.0 & \psi \geq 5.0
\end{cases}$$

(6)

Different random seed numbers are used to get different time series of wave heights, by assigning different phases to wave components during discretizing the wave spectrum.

The current loading is represented by a uniform current velocity distribution considering the effect of the boundary layer at the pipeline level and seabed roughness. Current velocity is given by Eq. (7) according to RP-F109 [16].

$$U_c = U_c(z_r) \cdot \left(\frac{1 + \frac{z_r}{z_0}}{2}\cdot \ln \left(\frac{D}{z_0} + 1\right) - 1\right) \cdot \sin(\theta_c)$$

(7)

where $U_c(z_r)$ is the current velocity at reference measurement height $z_r$ in a direction perpendicular to the pipeline, $D$ is the external pipeline diameter including all coatings, $z_r$ is the current reference measurement height above the seabed, $z_0$ is the seabed roughness parameter, and $\theta_c$ is the angle between current velocity direction and pipeline.

2.3 Hydrodynamic forces

The hydrodynamic forces which result from the wave and current loadings on the subsea pipeline are divided into horizontal and vertical forces. The horizontal forces result from the drag force ($F_D$) and the inertia force ($F_M$) and are calculated using Morison's equations [29] as given by Eqs. (8) and (9), respectively. The vertical forces result from the lift force ($F_L$) and are calculated as given by Eq. (10). The drag, inertia, and lift forces are directly applied in a direction perpendicular to the pipeline segment as distributed loads.

$$F_D = \frac{1}{2}\rho_w DC_D |U_r||U_r|$$

(8)

where $\rho_w$ is the mass density of the seawater, $D$ is the pipeline external diameter, $C_D$ is the coefficient of the drag force associated with the ambient flow passing the pipeline, and $U_r$ is the relative velocity between the fluid and the pipeline in a direction perpendicular to the
pipeline, \( U_t = (U_w + U_c - U_p) \), in which \( U \) is the total velocity of the water-particles contributed by the wave and current in a direction perpendicular to the pipeline: \( U = (U_w + U_c) \), and \( U_p \) is the pipeline velocity in a direction perpendicular to its span.

\[
F_M = \frac{1}{4} \rho_w \pi D^2 \left( C_M \frac{\partial U}{\partial t} - C_a \frac{\partial U_p}{\partial t} \right) \tag{9}
\]

where \( C_M \) is the coefficient of the inertia force associated with the ambient flow passing the pipeline, \( C_a \) is the coefficient of the added mass associated with the ambient flow passing the pipeline, \( C_a = (C_M - 1) \), \( \frac{\partial U}{\partial t} \) is the acceleration of the water particles contributed by the wave and water-current, and \( t \) is the computational time.

\[
F_L = \frac{1}{2} \rho_w D c_L (U - U_p)^2 \tag{10}
\]

where \( C_L \) is the coefficient of the lift force associated with the ambient flow passing the pipeline.

### 3 Case study

The case study, which is considered in this paper, represents a 22-in.-diameter pipeline, extending along the 250-m length, and subject to the combined effect of the two-dimensional irregular waves and steady current loads. The data of the pipeline, environment, and soil, upon which the present case study depends, is presented in the following subsections.

#### 3.1 Pipeline data

The pipeline with material grade API 5L X65 [5] has a geometric structural property, in the form of a rigid pipeline, associated with linear elastic structural properties. The pipeline data and material properties are presented in Table 1.

The pipeline is modeled as a single continuous line, which is restrained, as an initial position just above the seabed. A mesh is generated using a constant element length of 5 m throughout the pipeline length.

#### 3.2 Seabed and soil data

The seabed is considered as an elastic, flat surface, and without slope. The seabed soil is modeled as loose-to-medium sand, and it is defined by a single linear elastic stiffness. The longitudinal and transverse coefficients of the Coulomb friction model, as well as soil parameters, are presented in Table 2.

#### 3.3 Environmental data

The characteristics of the seawater, as well as the design data of the wave and current, corresponding to two return period values (RPV), are presented in Tables 3 and 4, respectively. The directions of the applied wave and current are assumed to be perpendicular to the pipeline.

#### 3.4 Boundary conditions

In the initial static analysis, both ends of the pipeline are assumed to be fixed in all translational and rotational degrees of freedom. An additional boundary condition is applied at regular intervals of 5 m along the pipeline to position the pipeline slightly hanging above the seabed.

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### Table 1 Pipeline data and material properties

| Parameter                  | Value  |
|----------------------------|--------|
| Pipe wall thickness        | 9.5 mm |
| Steel density              | 7850 kg/m³ |
| Young’s modulus            | 207 GPa|
| Specified minimum yield stress (SMYS) | 448 MPa |
| Poisson’s ratio            | 0.3    |
| Corrosion coating thickness| 3.2 mm |
| Corrosion coating density  | 950 kg/m³ |
| Concrete coating density   | 3040 kg/m³ |

### Table 2 Soil parameters

| Parameter                  | Value  |
|----------------------------|--------|
| Friction coefficient (\( \mu \)) | 0.6    |
| Soil stiffness              | 300 kN/m/m |
| Seabed roughness (\( z_0 \)) | 0.00001 m |

### Table 3 Sea characteristics

| Parameter                  | Value  |
|----------------------------|--------|
| Water depth (\( d \))      | 20 m   |
| Seawater density (\( \rho_w \)) | 1030 kg/m³ |
| Gravity acceleration (\( g \)) | 9.81 m/s² |
| Reference measurement height above the seabed (\( z_r \)) | 1 m |

### Table 4 Wave and current design data

| Parameter                  | Return period values (1 year, 10 years) |
|----------------------------|----------------------------------------|
| Peak period (\( T_p \))    | 13 s, 13.9 s                           |
| Significant wave height (\( H_s \)) | 2.4 m, 3.02 m                     |
| Current velocity (\( U_c(z_r) \)) | 0.23 m/s, 0.29 m/s                |
In the quasi-static analysis, all vertical constraints along the length of the pipeline are removed to allow for the pipeline to fall onto the seabed, under the combined influence of gravity and buoyancy, and to allow for the penetration of the pipeline into the soil.

In the dynamic analysis, the pipeline is assumed to be fixed in all translational and rotational degrees of freedom at the left end, whereas it is assumed to be fixed in all rotational degrees of freedom only at the right end.

3.5 Assumptions

• There is no temperature variation along the pipeline, to avoid the resultant excessive lateral displacements and bending moments.
• There is no deterioration in the thickness of the pipeline wall due to corrosion.
• A two-dimensional irregular wave system is considered satisfactory to represent the sea model.
• The coefficients of the hydrodynamic forces (i.e., inertia, drag, and lift) for a subsea pipeline resting on the seabed are assumed to be invariant during the whole analysis. According to DNV 1981 rules [14], and as reported by Verley et al. [42], the inertia, drag, and lift coefficients are taken as equal to 3.29, 0.7, and 0.9, respectively.
• All added coating layers increase the weight per unit length for the pipeline only, but they do not contribute to its stiffness.
• The concrete coating thickness increment is 5 mm.
• During the first 100 s of the simulation, the wave loads are allowed to increase from zero to full value, by applying a linear ramp function according to RP-F109 [16].
• The effect of the cyclic loads on the embedment of the pipeline into the soil is not considered because of using linear soil stiffness.

4 Results

The dynamic on-bottom stability analysis is conducted using Flexcom software to determine the required concrete coating thickness which satisfies the stability of the pipeline against the applied hydrodynamic loads and to investigate the dynamic pipeline response. Several simulation runs are performed under different loading combinations from waves and steady currents using (fixed) and (random) seed numbers, and different concrete coating thicknesses. To minimize the number of dynamic simulation runs, the initial guess of concrete coating thickness required for stability was determined using the ALSS method and considered to be the basis of conducting the dynamic analysis to minimize the number of dynamic simulation runs.

The acceptance criteria, which are used in this case study, can be summarized in two principal directions as follows: to achieve a relatively stable pipeline, i.e., to keep the lateral displacement of the pipeline less than half of its external diameter \(D\), and to keep the resultant stresses within their allowable limits. In this case study, the allowable limit of the von Mises stress is taken as 430 MPa (i.e., 96% of the SMYS). The resultant stresses are to be checked thoroughly to avoid excessive loading effects such as bending moments which may affect the integrity of the pipeline by causing local buckling or collapsing of the pipeline wall.

4.1 The combined load of 1-year RPV wave + 10-year RPV current

Under the action of the combined loading condition of 1-year RPV wave + 10-year RPV current, and for a concrete coating thickness less than or equal to 145 mm, the pipeline records an instability as shown in Fig. 3, and the lateral displacements recorded are beyond the allowable limit.

The von Mises stresses corresponding to the preceding lateral displacements are presented in Fig. 4. The associated stresses do not exceed the allowable limit, except the stresses recorded at a concrete coating thickness of 140 mm. For this range of concrete coating thicknesses (less than or equal to 145 mm), both design criteria (displacements and stresses) are not satisfied, which necessitates increasing the stability weight.

By increasing the concrete coating thickness, the pipeline becomes relatively stable at a concrete coating thickness greater than or equal to 155 mm as shown in Fig. 5. The von Mises stresses corresponding to these lateral displacements do not also exceed the stress allowable limit as shown in Fig. 6. Therefore, the design criteria (displacements and stresses) are satisfied for concrete coating thicknesses greater than or equal to 155 mm.

4.2 The combined load of 10-year RPV wave + 1-year RPV current

Under the action of the combined loading condition of 10-year RPV wave + 1-year RPV current, and for a concrete coating thickness less than or equal to 165 mm, the pipeline records an instability as shown in Fig. 7. And the lateral displacements recorded are beyond the allowable limit.

The von Mises stresses corresponding to these lateral displacements are not also exceed the stress allowable limit as shown in Fig. 8. Therefore, the design criteria (displacements and stresses) are satisfied for concrete coating thicknesses greater than or equal to 155 mm.
160 mm. For this range of concrete coating thicknesses (less than or equal to 165 mm), both design criteria (displacements and stresses) are not satisfied, which necessitates increasing the stability weight.

By increasing the concrete coating thickness, the pipeline becomes relatively stable as shown in Fig. 9. The von Mises stresses corresponding to these lateral displacements are also within the specified allowable limit as shown in Fig. 10. Accordingly, both design criteria...
(displacements and stresses) are satisfied for concrete coating thicknesses greater than 170 mm.

4.3 Pipeline response investigation

In this numerical investigation, the first 3000 s only of the time-domain simulation of the pipeline right end is considered to investigate the pipeline response. Based on the numerical results shown in Fig. 9, and for a
concrete thickness equal to 180 mm, the time history of the lateral and vertical displacements and the total velocity of the water particles is presented in Figs. 11, 12, and 13, respectively.

Figure 11 shows that the pipeline right end experiences highly oscillatory lateral displacements at certain time intervals (e.g., at 898, 1417, 2054, and 2452 s). The same is shown in Fig. 12 that the right end also experiences highly oscillatory vertical displacements for the
same time intervals as in the case of the oscillatory lateral displacements.

The principal reason behind these lateral and vertical displacements is reverted to the drag, inertia, and lift forces which are induced under the action of the total water particles velocity at the pipeline level. As shown in Fig. 13, the total water particles velocity has few peak values at the same time intervals, which in turn increases the hydrodynamic forces affecting the pipeline and results in these lateral and vertical displacements.

Fig. 9  Envelopes of the lateral displacements of the pipeline for concrete thickness range 170–180 mm (10-year RPV wave + 1-year RPV current)

Fig. 10  Envelopes of the von Mises stresses of the pipeline for concrete thickness range 170–180 mm (10-year RPV wave + 1-year RPV current)
Fig. 11  Time history of the lateral displacement for the pipeline right end for 180 mm concrete coating thickness

Fig. 12  Time history of the vertical displacement for the pipeline right end for 180 mm concrete coating thickness
4.4 Random seed numbers
The numerical results obtained in the previous sections are based on a single seed number, i.e., the same phase shift is assigned to all wave components constituting the irregular wave system, for all simulation runs. Indeed, to ensure the stability of the pipeline under the action...
of various irregular sea states, different seed numbers should be used. RP-F109 [16] recommends performing seven simulation runs at least with randomly chosen seed numbers, to consider the effect of the different heights of the irregular waves on the pipeline dynamic response. Based on the numerical results, it is observed that the load combination of 10-year wave + 1-year current represents the worst loading condition, as is already indicated by the high concrete coating thickness required for pipeline stabilization. Therefore, this loading condition is selected to perform seven simulation runs at a concrete coating thickness equal to 180 mm.

Figure 14 shows the results for lateral displacements corresponding to different irregular sea states based on randomly selected seed numbers. The maximum lateral displacement of the pipeline has occurred at seed numbers 1 and 2, and both values exceed the allowable limit which indicates the importance of performing seven simulation runs using randomly selected seed numbers. However, the von Mises stress values are satisfying the stress limit criterion for the same irregular sea states as shown in Fig. 15.

It is observed that the induced stresses are increased in the region nearby the left fixed end because of the boundary condition at the left end of the pipeline. Therefore, the induced stresses at a location of 75 m from the left end of the pipeline satisfactorily represent the von Mises stresses.

### Table 5 Results of comparison between DLS, ALSS, and GLS methods

| Load combination | Concrete coating thickness results (mm) |
|------------------|----------------------------------------|
|                  | DLS using Flexcom | ALSS | GLS |
| 1-year RPV wave + 10-year RPV current | 155–160 | 161 | 70 |
| 10-year RPV wave + 1-year RPV current | 170–180 | 230 | 79 |

#### 4.5 Comparison with conventional stability methods

Ignoring the passive soil resistance term in the present DLS numerical calculations and analysis entails the necessity of studying its effect on the dynamic response of the pipelines. This study may be achieved by comparing the present DLS numerical results against those of the other conventional stability methods (e.g., ALSS and GLS) provided in RP-F109 [16].

Table 5 shows the required concrete coating thickness which is necessary for stabilizing the subsea pipeline based on each method of stability; it is observed that both DLS and ALSS methods result in relatively high concrete coating thickness in comparison with the GLS method because of ignoring the passive soil resistance term. It is observed also that DLS analysis results in less concrete coating thickness in comparison with ALSS method despite ignoring the passive soil resistance. This
proves that the DLS analysis method can optimize the on-bottom stability design of the subsea pipelines and results in less concrete weight coating if the actual case is modeled correctly.

5 Discussion
The soil resistance was modeled using the pure friction term in between the soil and the pipeline, which was represented by the Coulomb friction model, but it did not consider the passive resistance of the soil due to the embedment of the pipeline, because of the present capabilities of the software.

Ignoring the passive soil resistance term has limited the acceptance criteria for lateral displacement to 0.5D instead of 10D because of uncontrolled lateral displacement and the simplicity of the soil model that is based on the Coulomb friction model.

The absence of passive soil resistance can be clearly noticed by recording either the lateral displacement of the pipeline nodes or the rapid change in pipeline stability. Obviously, the right end laterally displaces steadily in proportion to the applied hydrodynamic forces if the latter exceed the soil resistance force as shown in Fig. 11. The absence of passive soil resistance can also be noticed from the rapid change in pipeline stability with increasing its weight as shown in Figs. 7 and 9.

With regard the comparison with conventional stability methods presented in RP-F109 [16], It is worth to highlight that both ALSS and GLS methods consider the effect of the passive soil resistance implicitly. The ALSS design method considers an initial embedment of the pipeline into the soil but does not consider the effect of any increment in the passive soil resistance due to any further embedment actioned by the hydrodynamic cyclic loading on the pipeline [2]. The GLS design method considers the effect of passive soil resistance based on design curves with non-dimensional parameters presented in RP-F109 [16]. These design curves are extracted from finite element dynamic simulations following the recommendations of dynamic lateral stability of the pipeline on the a flat seabed.

6 Conclusions
The paper investigates numerically the dynamic on-bottom lateral stability of a concrete-coated subsea pipeline using one of the available offshore simulation software, namely Flexcom [46]. Flexcom was used to model the pipeline in the realistic sea state, which is composed of a combination of irregular waves and steady currents.

The time-domain simulation of the DLS of a subsea pipeline offers a better understanding of its response, in addition to a clear prediction of the limits of its lateral displacements and associated stresses. Compared to the conventional pipeline stability approaches, this type of analysis is very time-consuming and generally requires many details to accurately model the in situ subsea pipeline, using a finite element model. A brief discussion of the main conclusions that may be aggregated from this paper is:

- If the joint probability distribution of the waves and currents is unavailable, then the most-worse loading combination of RPV of waves and currents shall be applied as recommended by RP-F109 [16].
- Hydrodynamic loads from drag, inertia, and lift forces generated on the pipeline are increased by increasing the total water particle velocity induced from the summation of wave-induced particle velocity and current velocity.
- Ignoring the passive soil resistance term decreases the soil resistance dramatically and pipeline weight becomes the major factor in the assessment of on-bottom stability analysis, especially when considering the pipe–soil interaction in terms of pure friction term only. Ignoring passive soil resistance also increases the concrete weight requirement markedly which increases line pipes manufacturing and installation costs.
- Increasing pipeline weight increases the contact force on the seabed and hence increases soil resistance to the lateral displacement. Therefore, all mathematical models, which are based on the pure friction term, mostly result in conservative weights of stability.
- In the critical cases in which the lateral displacements exceed their allowable limits, the stresses induced by such excessive lateral displacements should be thoroughly examined to ensure pipeline integrity. Excessive stresses (such as bending moments) may result in collapsing the pipe wall, in consequence losing its integrity.
- Random seed numbers assigned to wave components have an impact on confirming the choice of the concrete coating thickness. Seven simulation runs with seven randomly chosen seed numbers should be performed as recommended by RP-F109 [16].

Abbreviations
AGA: American Gas Association; ALSS: Absolute lateral static stability; API: American Petroleum Institute; DLS: Dynamic lateral stability; DNV: Det Norske Veritas; DNVGL: Det Norske Veritas–Germanischer Lloyd; FEA: Finite element analysis; FE: Finite element; GLS: Generalized lateral stability; JONSWAP: Joint North Sea Wave Project; RP: Recommended practice; RPV: Return period
values; SMYS: Specified minimum yield stress; PRCI: Pipeline Research Council International.

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Authors’ contributions
KAH communicated to the software developers to get the license. MAA built the numerical model, performed the numerical simulation, interpreted the results, and drafted the manuscript. KAH and ANA supervised the research work and critically revised the manuscript. All authors reviewed the results and approved the final version of the manuscript.

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Declarations

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Not applicable.

Consent for publication
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Competing interests
The authors declare that they have no competing interests.

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