Abstract

Description of a new model of the Solar System is given in this paper. Analogously to the planetary atomic model of Rutherford, we describe an Atomic Model of the Solar System (AMSS) in which the planets are coupled like electrons in atoms. The AMSS presented put into evidence the existence of a tenth celestial object (nicknamed here SENEG) that might be the centuries-long searched tenth planet or classified in the category of dwarf planets. Since the much controverted Prague (IAU0603 2006) statement, astronomers actively search beyond Neptune a probable ninth planet. The AMSS model gives in the viewpoint of mathematics, the criterion satisfied by a planet belonging to the Solar System. The AMSS indicates that, the stability of the Solar System is only compatible with a configuration containing ten planets and that SENEG orbits the Sun at the distance of 11,208,000,000 km. From the AMSS model, it is mathematically shown that both 2003 VB12 (Sedna) and 2003 UB313 (Xena) have not the status of planets and they may be classified in the category of dwarf planets. Discussion about how the AMSS model may play a prominent role in the implementation of the quantum theory of freedmons is also made.

Keywords:
Solar system; Dwarf planets; Atomic model of the solar system; Freedmon

Introduction

In the absence of an exact theory on the Solar System, one can only perform planetary models based on a certain number of simplified hypotheses. Each of these approximate models gives only a partial information of the granularly structure of the Solar System. In the past, nine planets (from Mercury to Pluto) have been discovered as belonging to the Solar System. Formerly, two new ‘planets’ referred as 2003 VB12 [1] and 2003 UB313 [1-3] have been discovered and considered as belonging to the Solar. During the 26th general assembly of International Astronomical Union (IAU) which has took place on the 14 and 25 of August 2006 at Prague, Pluto has been declined of its status of planet [4]. Since the much-controverted Prague (IAU0603 2006) statement, astronomers actively search beyond Neptune a probable ninth planet [5]. Obviously, the number of planets of the Solar System is not infinite. Subsequently, it would be very challenging in the view point of mathematics, to establish the criterion satisfied by a planet belonging to the Solar System. In addition, the stability of the Solar System depends on its number of planets and on how these planets are configured in the planetary cloud of the Sun. The centrifugal force due to the orbital motion of a planet may not be sufficient to counterbalance the attractive gravitational force from the Sun. That means, the stability of the orbit of a given planet of the Solar System is probably due to additional strong attractive planet-planet interaction. This assumption suggests to consider a configuration in which the planets are coupled like electrons in atoms. So attractive interaction between two coupled planets contributes to their stability and to that of the whole Solar System. In the past, Rutherford managed to explain the stability of the atomic systems by proposing a planetary model of the atom. Adopting an opposite procedure to that of Rutherford, we describe an atomic model of the Solar System (AMSS) putting into evidence the existence of a tenth celestial object (that may be a planet or a dwarf planet). We assume that, at a certain moment of its formation, the Solar System captured a tenth celestial object for its stability. In the framework of the AMSS model, the planets orbiting the Sun are then coupled. On the other hand, it’s generally believed that, the only sure method to identify the tenth planet is to know its exact situation in the firmament and then to discover it at the indicated place [6]. The following study is in this direction. In section 2 we present our atomic model of the Solar System. In section 3 the presentation and the discussion of our results are made. Comparison is also done with available astronomical observations.

Theory

Some similarities between the Solar System and the atomic systems

In the following study, we adopt the model of the independent particles that disregards planet–planet interaction and electron–electron interaction. Then, for a given system (astronomic or atomic), direct interaction of the particle (planet or electron) with the center of the system (Sun or Nucleus) is considered. We use also the model of the Copernican Solar System and the Bohr’s atomic model in the approximation of the circular orbit of the particles (planets or electrons respectively). In Table 1, some elements of comparison are displayed. These elements listed in Table 1 show without doubt that there is no contradiction between the macrocosm and the microcosm. How then one can explain discrepancies between the Solar System and the atomic systems in view of the analogical elements quoted in the seventeenth and eighteenth lines of Table 1? Nothing could logically explain that. Then we assume that, like electrons in atoms, the planets in the Solar System are coupled. As a result, Pluto might be coupled to a tenth celestial object (planet or dwarf planet).
In these ratios, \( n \) denotes the rank of the inner coupled planet with respect to the Sun, \( V, d \) and \( T \) represent respectively the orbital speed, the average distance to the Sun and the period of the orbital motion of the considered planet. By use of the values quoted in Table 2, we find:


\[
\frac{V_{n+1}}{V_n} = \left( \frac{d_{n+1}}{d_n} \right)^{1/2} \quad \text{and} \quad \left( \frac{T_{n+1}}{T_n} \right)^2
\]

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\[\begin{align*}
\frac{V_{n+1}}{V_n} & = \left( \frac{d_{n+1}}{d_n} \right)^{1/2} \quad \text{and} \quad \left( \frac{T_{n+1}}{T_n} \right)^2 \\
\end{align*}\]

For the cubic ratios of the average distance with respect to the Sun (Table 3):

\[\begin{align*}
\left( \frac{d_{n+1}}{d_{n}} \right)^3 & = \left( \frac{108.14}{57.84} \right)^3 = 6.535; \quad \left( \frac{d_{n+1}}{d_{n}} \right)^3 = \left( \frac{1426}{777.8} \right)^3 = 6.162 \\
\left( \frac{d_{n+1}}{d_{n}} \right)^3 & = \left( \frac{227.8}{149.5} \right)^3 = 3.537; \quad \left( \frac{d_{n+1}}{d_{n}} \right)^3 = \left( \frac{4494}{2868} \right)^3 = 3.847
\end{align*}\]

For the square ratios of the orbital motion period:

\[\begin{align*}
\left( \frac{T_{n+1}}{T_n} \right)^2 & = \left( \frac{19.4}{7.6} \right)^2 = 6.515; \quad \left( \frac{T_{n+1}}{T_n} \right)^2 = \left( \frac{9.3}{3.74} \right)^2 = 6.183 \\
\left( \frac{T_{n+1}}{T_n} \right)^2 & = \left( \frac{5.94}{3.16} \right)^2 = 3.533; \quad \left( \frac{T_{n+1}}{T_n} \right)^2 = \left( \frac{5.20}{2.66} \right)^2 = 3.821
\end{align*}\]

Considering the preceding results, we deduce the simple following laws.

First law: Law of variation of the ratio of the average orbital speed of the coupled planets

For a couple of planets considered, if \( n \) denotes the rank of the inner planet of the couple with respect to the Sun, the ratios of their average orbital speed satisfy the condition,

\[\frac{V_{n+1}}{V_n} = \lambda_n \quad \text{with} \quad \lambda_n = \begin{cases} 0.73 & \text{if } n \text{ is odd} \\
0.80 & \text{if } n \text{ is even} \end{cases}\]

Second law: Law of variation of the ratio of the average distance to the Sun of the coupled planets

For a couple of planets considered, if \( n \) denotes the rank of the inner planet of the couple with respect to the Sun, the ratios of their average distance to the Sun satisfy the condition,

\[\frac{d_{n+1}}{d_n} = d_n^{0.71} \quad \text{with} \quad d_n = \begin{cases} (\text{max} \text{imum}) & \text{or} & (\text{min} \text{imum}) \text{ if } n \text{ is odd} \\
4(\text{max} \text{imum}) & \text{or} & 3(\text{min} \text{imum}) \text{ if } n \text{ is even} \end{cases}\]

Third law: Law of variation of the ratio of the average period of the orbital motion of the coupled planets

For a couple of planets considered, if \( n \) denotes the rank of the inner planet of the couple with respect to the Sun, the ratios of their average period of the orbital motion satisfy the condition (Table 3).
Results and Discussion

According to the AMSS model, the tenth celestial object nicknamed SENEG is coupled to Pluto.

Average orbital speed of the tenth celestial object

Using the first law (7), we find,

\[
\frac{V_{\text{seneg}}}{V_{\text{pluto}}} = \frac{V_{\text{seneg}}}{V_{\text{pluto}}} = \lambda_0 = 0.73
\]

As \(V_{\text{pluto}} = 4.73\) km/s, equation (9) gives for SENEG,

\[
V_{\text{seneg}} = 3.45\text{ km/s}
\]

Framing of the average distance of the tenth celestial with respect to the Sun

As it can be noticed in the formulation of the second law (8), only a framing of the average distance of the tenth celestial object with respect to the Sun can be rigorously established. Then according to this law, we find

\[
6 < \left( \frac{d_{\text{seneg}}}{d_{\text{pluto}}} \right)^2 \frac{1}{7}
\]

As \(d_{\text{pluto}} = 5908\) 10³ m, double inequality (11) gives,

\[
10735 \times 10^3 < d_{\text{seneg}} < 11302 \times 10^3
\]

In astronomical unity 1AU = 149.5 10³ m, the result (12) becomes,

\[
1.81\text{ AU} < d_{\text{seneg}} < 1.75\text{ AU}
\]

But as the average orbital speed \(V\) and the average distance \(d\) of a planet are linked by the well known formula:

\[
V = \sqrt{\frac{GM}{d}}
\]

where \(G\) denotes the gravitation constant and \(M\) the mass of the Sun.

In the basis of \(G = 6.67 \times 10^{-11}\text{ SI} ; M = 2 \times 10^{30}\text{ kg} \) and \(V_{\text{seneg}} = 3.45\text{ km/s} \), equation (14) gives,

\[
d_{\text{seneg}} = 11208\text{ km}
\]

This result agrees well with the condition (12).

Framing of the average period of the orbital motion of the tenth celestial object

By use of the third law we find,

\[
6 < \left( \frac{T_{\text{seneg}}}{T_{\text{pluto}}} \right) < 7
\]

As \(T_{\text{pluto}} = 7.82\times 10^9\text{ s} \), double inequality (16) gives,

\[
9.15 \times 10^9 < T_{\text{seneg}} < 20.69 \times 10^9\text{ s}
\]

On the other hand, \(d\) and \(T\) are linked by the third law of Kepler,

\[
T^2 = \frac{4\pi^2}{GM} \frac{d^3}{d_{\text{seneg}}^3}
\]

Using the value (15) of \(d_{\text{seneg}}\), equation (18) gives for \(T_{\text{seneg}}\) the result,

\[
T_{\text{seneg}} = 20.52\text{ AU}
\]

This result agrees well also with the condition (17).

For comparison, let us remind former astronomical observations. In the past, a group of five comets have been discovered and their aphelia are about 50,800,000,000 km of the Sun. This localises them around the orbit of Pluto. In addition, for sixteen identified comets, the
aphelia is situated to more than 11,000,000,000 kilometres of the Sun [6,7]. As most of things relative to the Solar System, the progression of the Bode’s law [8,9] (Table 4) considered especially as an amusing curiosity supposed that the sixteen identified comets which the aphelia is at 11,000,000,000 kilometres of the Sun are dominated by a tenth planet who follows an orbit with an average distance to the Sun equals to this aphelia [6]. The preceding astronomical observations agree well with our theoretical result (15). This indicates that, the tenth celestial object might be researched among the sixteen formerly identified comets which the aphelia is at more than 11,000,000,000 kilometres of the Sun (Table 4).

**Consequences from AMSS**

Is 2003 VB12 (Sedna) or 2003 UB313 (Xena) the hypothetical tenth planet? In the year 2003, astronomical observations have instituted debates between two planets supposed to be the tenth planet. Astronomers at California Institute of Technology, manage then to identify by use of Samuel Oschin Telescope (Palomar mount) two planets assumed to belong to the Solar System. These planets were baptized 2003VB12 (Sedna) and 2003UB313 (Xena) [3,4,7].

Table 4: Comparison of the distance of the ninth planets of the solar system with the predictions of the Bode’s law.

| Name of the celestial object | Average distance Planet-Sun | Average distance Planet-Sun According to the Bode’s law* |
|-----------------------------|-----------------------------|--------------------------------------------------------|
| Mercury                     | 0.39                        | 0.4                                                    |
| Venus                       | 0.72                        | 0.7                                                    |
| Earth                       | 1.0                         | 1.0                                                    |
| Mars                        | 1.52                        | 1.6                                                    |
| Asteroids                   | 2.65 (approx.)              | 2.8                                                    |
| Jupiter                     | 5.2                         | 5.2                                                    |
| Saturn                      | 9.64                        | 10                                                     |
| Uranus                      | 19.19                       | 19.6                                                   |
| Neptune                     | 30.05                       | 38.8                                                   |
| Pluto                       | 39.52                       | 77.2                                                   |

*Robert [8].

All values are reported in UA: 1 UA = 149.5 × 10^9 m.

The distances of these two planets with respect to the Sun are respectively equal to 91 UA and 97 UA [3,4,7]. Let’s us calculate for each of them the ratio (d/1UA)^3. We find respectively:

\[
\left( \frac{d_{2003\,VB12}}{d_{\text{Plan}}} \right)^3 = \frac{90}{39.52} = 11.811
\]

(20)

\[
\left( \frac{d_{2003\,UB313}}{d_{\text{Plan}}} \right)^3 = \frac{97}{39.52} = 14.786
\]

(21)

These results show that the condition (11) is not satisfied. Then both 2003 VB12 and 2003 UB313 cannot have the status of a planet. This result matches well with what is accepted for their celestial bodies classified in the category of Ceres in motion between Mars and Jupiter and are then considered as dwarf planets [7]. Let us know turn on debating the Prague statement considering the Solar System as composed of eight planets, both Pluto and 2003 UB313 being dwarf planets category [7]. According to the new definition, two conditions must be satisfied for an object to be called a “planet.” Firstly, the object must be in orbit around a star, while not being itself a star. Secondly, the object must be large enough (or more technically correct, massive enough) for its own gravity to pull it into a nearly spherical shape. The shape of objects with mass above 5 ×1020 kg and diameter greater than 800 km would normally be determined by self-gravity, but all borderline cases would have to be established by observations [4]. Then, it is on the basis of the new definition of a planet that Pluto has been dethroned since 2006. As the planetary model of the atom is correct, the atomic model of the Solar System merits attracting attention by the only fact that it will help physicists and astronomers to find the way for conciliating the macrocosm and the microcosm [6,7]. The three laws established above indicate that the planets are probably coupled and then can be considered as the main credit of the validity of our AMSS. As both 2003 VB12 and 2003 UB313 are not coupled to Pluto, legitimately SENEG might be the celestial body of the Solar System coupled to Pluto and they might have the same status (planet or dwarf planet). This means that, if SENEG is a planet, the status of Pluto will be restored as a planet. Subsequently, the discovery of SENEG by photography using for instance the Samuel Oschin Telescope at Palomar Observatory, will involve inevitably a reevaluation of the Prague 2006 statement as far as the status of Pluto is concerned [9,10].

**About the quantum theory of freedmon:** As emphasize by Ginzburg [11,12], “For a distant exterior observer, the whole world can appear like a small particle, a freedmon. In the framework of the classical theory, the mass, the charge and the other parameters (the spin) of the freedmon have not been yet determined and the quantum theory of freedmons is not yet established. However, one can hope that, in the quantum theory, freedmons possess parameters of the elementary particles. At present hour, it is a fantastic eventuality, a hope, a dream. But it merits attracting attention by the only fact that it will help physicists to find the way for conciliating the contradictions (the macrocosm and the microcosm)”.

According to our atomic model of the Solar System, the planets are coupled and might have quantum angular momentum of spin like electrons. The AMSS model presented suggests considering each planet as a freedmon of spin ½. In fact, the concept of spin is borrowed to the word spinning which means turning around its own axis like a classical spinning top. As all planets are spinning, one can well assume legitimately that they are characterized by an angular momentum of spin. If the planetary system is equal to that of the electron (1/2), this will be a great path toward the way leading to the unification of the macrocosm and the microcosm. We hope that our atomic model of the Solar System will greatly help in the development of the quantum theory of freedmons. Previously, we have demonstrated the possibilities to understand the organization and the evolution of astronomical systems by dealing with analogy between the properties of elementary particles and astrophysical objects [10-12]. The quantum theory of freedmons might be the more exciting astrophysical topic in the forthcoming decade.

**Conclusion**

With a simple atomic model of the Solar System, we have putted into evidence the existence of a tenth “planet” for the stability of the
Solar System. The model presented in this work permits the calculation of the distance of the tenth planet with respect to the Sun which is the principal characteristic for identifying it in the firmament. The present study has also the merit to fix the conditions to be satisfied by a planet belonging to the Solar System. This point is extremely important as it is obvious that the Solar System cannot contain infinite celestial objects. On the other hand, the similarities shown in this paper through Table 1 between atomic configurations and the Solar System indicate that our atomic model of the Solar System may play an important role in the implementation of the quantum theory of freedmons. We name temporary SENEG as the tenth celestial object coupled to Pluto. In August 2006, the IUA stated that, a planet of the Solar System is a celestial body which at least is in orbit around the Sun and has sufficient mass to assume hydrostatic equilibrium. As the mass of SENEG is not known for the time being, it is not possible to state to its status of a planet or a dwarf planet.

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