Optical cavities transmit light only at discrete resonant frequencies, which are well-separated in microstructures. Despite attempts at the construction of planar ‘white-light cavities’, the benefits accrued upon optically interacting with a cavity – such as resonant field buildup – have remained confined to narrow linewidths. Here, we demonstrate achromatic optical transmission through a planar Fabry-Pérot micro-cavity via angularly multiplexed phase-matching that exploits a bio-inspired grating configuration. By correlating each wavelength with an appropriate angle of incidence, a continuous spectrum resonates and the micro-cavity is rendered transparent. The locus of a single-order 0.7-nm-wide resonance is de-slanted in spectral-angular space to become a 60-nm-wide achromatic resonance spanning multiple cavity free-spectral-ranges. The result is an ‘omni-resonant’ planar micro-cavity in which light resonates continuously over a broad spectral span. This approach severs the link between the resonance bandwidth and the cavity-photon lifetime, thereby promising resonant enhancement of linear and nonlinear optical effects over broad bandwidths in ultrathin devices.

Optical cavities are a cornerstone of photonics. They are indispensable in lasers, optical filters, optical combs and clocks, in quantum physics, and have enabled the detection of gravitational waves. Optical-cavity resonances occupy narrow spectral linewidths that are inversely proportional to the cavity-photon lifetime, which are separated by a free spectral range (FSR) that is inversely proportional to the cavity size. Although cavity-quantum electrodynamics requires narrow cavity linewidths to isolate the interaction of optical fields with the resonances of atoms, ions, or nanostructures, most applications would benefit from maintaining the resonant cavity-field-buildup over an extended bandwidth. Examples of such applications include coherent perfect absorption (CPA) in media endowed with low intrinsic losses and boosting nonlinear optical effects. Although CPA, for instance, can increase absorption to 100% in a thin low-loss layer, exploiting CPA in harvesting solar radiation would require an optical cavity in which an extended bandwidth satisfies the resonance condition.

The quest for producing an achromatic resonator has precedents. In ‘white-light cavities’, the cavity itself is modified by inserting a new material or structure endowed with strong negative (anomalous) dispersion to equalize the cavity optical length for all wavelengths. Only macroscopic white-light cavities have been explored to date via cavity-filling atomic species featuring bifrequency Raman gain in a double-λ system or displaying electromagnetically induced transparency, or alternatively via nonlinear Brillouin scattering. In all such studies, the enhanced cavity linewidths are extremely narrow (~100 MHz or <1-pm-wide) by virtue of the very nature of the atomic or nonlinear resonances utilized, and are limited by uncompensated higher-order dispersion terms. Alternative approaches based on the use of linear optical components, such as appropriately designed chirped mirrors or grating pairs, have been investigated. Surprisingly, both of these possibilities fail at producing a white-light cavity due to subtle overlooked aspects in the constraints imposed by causality on non-dissipative systems. A different approach in the context of whispering gallery modes in a micro-cavity relies on increasing the modal density by enlarging the cavity volume. First, increasing the cavity diameter reduces the free-spectral range (by increasing the number of modes identified by the azimuthal index) while retaining the high cavity finesse; and, second, the enlarged cavity thickness introduces new modes in the orthogonal dimension. The combination of the resonances of different spatial modes creates a flat spectral response by virtue of their spectral overlap upon proper coupling of light to the cavity.

Here we demonstrate achromatic transmission through a planar Fabry-Pérot micro-cavity – not via a modification of its structure, but instead by altering the spectral-angular configuration of the incident optical radiation using linear optical components. We show that the spatial degree-of-freedom of the optical field when used in conjunction with its spectral degree-of-freedom altogether obviates the limitations inherent in...
Figure 1. Spectral-angular correlations produce achromatic resonances in a micro-cavity. (a) When collimated broadband light is incident normally on a planar Fabry-Pérot cavity (top row), only a discrete set of wavelengths transmit (middle row) whose axial component of the wave vector inside the cavity is an integer multiple of \( k_0 = \pi/d \) (identified by solid horizontal dashes in the bottom row); \( \delta \lambda \) is the resonance linewidth. (b) The cavity resonances are blue-shifted when light is incident at an angle \( \theta \). (c) By assigning each wavelength \( \lambda \) to an appropriate angle of incidence \( \theta(\lambda) \), all the wavelengths can resonate and transmission becomes achromatic. One resonant order can extend here over a bandwidth exceeding the FSR. (d) Locus of resonant orders in spectral-angular space. Fixing the angle of one wavelength \( \theta(\lambda_0) \), we can de-slant the resonance of a specific order (colored curve) by boosting and reducing a pre-compensation angle for each wavelength to produce an achromatic resonance (solid horizontal line). An angular spread \( \Delta \theta \) at the input is required to de-slant the resonance between \( \lambda_3 \) and \( \lambda_5 \). At the shorter wavelength \( \lambda_5 \), the incidence angle needs to be increased above \( \theta(\lambda_5) \) by \( \theta(\lambda_5) - \theta(\lambda_3) \). The longer wavelength \( \lambda_3 \) requires an incidence angle lower than \( \theta(\lambda_3) \) by \( \theta(\lambda_5) - \theta(\lambda_3) \). Consequently, \( \lambda_3, \lambda_5, \theta_3 \), and \( \theta_5 \) all satisfy the resonance condition.

The concept of an achromatic resonance

The underlying physical principle for realizing an omni-resonant planar Fabry-Pérot cavity can be understood by referring to Fig. 1. At normal incidence [Fig. 1a], only discrete wavelengths resonate whose associated roundtrip phase \( \varphi \) is an integer multiple of \( 2\pi \), \( \varphi(\lambda) = 2nkA + 2\gamma(\lambda) = 2\pi m; \) here \( \lambda \) is the free-space wavelength, \( k = 2\pi/\lambda \) is the wave number, \( d \) and \( n \) are the thickness and refractive index of the cavity layer, respectively, integer \( m \) is the resonant-mode order, and \( \gamma \) is the reflection phase from the cavity mirrors' (assumed symmetric). At an incidence angle \( \theta \), the resonances are blue-shifted [Fig. 1b] because only the axial component of the wave vector contributes to the phase \( \varphi(\lambda, \theta) = 2nkA \cos \theta' + 2\gamma(\lambda, \theta') = 2\pi n \), where \( \theta' \) is the angle inside the cavity corresponding to an external angle \( \theta \). Indeed, for every wavelength \( \lambda \), there is an angle \( \theta(\lambda) \) that enables this particular wavelength to resonate by satisfying the phase-matching condition

\[
\varphi(\lambda, \theta) = 2nkA \cos[\theta'(\lambda)] + 2\gamma(\lambda, \theta') = 2\pi n. \tag{1}
\]

Therefore, re-organizing the incident broadband radiation by assigning each wavelength \( \lambda \) to an appropriate incidence angle \( \theta(\lambda) \) enables all the angularly multiplexed wavelengths to resonate simultaneously [Fig. 1c], with shorter wavelengths requiring larger incidence angles. Hence, by providing a pre-compensation tilt angle to each wavelength prior to incidence, such that \( k \cos \theta(\lambda) \) is constant, we effectively de-slant the resonance by maintaining \( \varphi(\lambda, \theta) \) independent of \( \lambda \) [the horizontal line in Fig. 1d].

We first present a heuristic argument for the construction of an optical system that de-slants a resonance in spectral-angular space [Fig. 2a]. A ‘black box’ system that implements any of the targeted correlations \( \theta(\lambda) \) shown...
in Fig. 2b will enable a broadband beam to transmit through the cavity via angular multiplexing – with all the wavelengths resonating simultaneously – and then its inverse restores the original beam. Dispersive prisms do not provide the required angular spread, and planar surface gratings produce the opposite correlation: longer wavelengths diffract at larger angles with respect to the normal as a consequence of transverse phase-matching [dashed curve in Fig. 2b]24. In other words, the spatial-spectral dispersion inculcated by an optical grating and by a cavity are in opposition. Instead, so-called ‘anomalous diffraction’ or ‘reverse-color sequence’ is required.

To address this challenge, we take our inspiration from the reverse-color sequence observed in the diffraction of white light off the wing scales of the butterfly Pierella luna21. This effect has been revealed to be geometric in nature: ‘vertical’ micro-gratings that grow on the Pierella luna scales reverse the sequence of diffracted colors as confirmed by fabricated artificial counterparts22. We adopt this strategy here in reflection mode and vary the relative tilt between the grating and the cavity, from 0° in Fig. 2c to 90° in Fig. 2d, to enable a transition from normal to anomalous diffraction, respectively.

To gain insight into the resonance de-slanting procedure, we first examine the spectral-angular variation in the axial wave-vector component $k_z$ of broadband light propagating in a bulk planar layer of refractive index $n$. Consider a bandwidth $\Delta \lambda$ centered at $\lambda_c$ and each wavelength is directed at a different angle $\theta(\lambda)$, with $\theta(\lambda_c) = \psi$, such that the beam occupies an angular spread $\Delta \theta$ (assume the wavelengths are distributed uniformly around $\psi$).

For a wavelength $\lambda$ incident at an external angle $\theta$, $k_z$ in the layer is

$$k_z(\lambda, \psi; \beta) = \frac{2\pi}{\lambda} \sqrt{n^2 \sin^2 \theta - \sin^2 \theta(\lambda - \lambda_c)},$$

where $\beta = \Delta \theta/\Delta \lambda \text{ nm}$ is the angular dispersion, we take $n = 1.5$ and $\lambda_c = 550 \text{ nm}$, and we ignore the spectral variation of $n$ for simplicity. We search for a region in $(\lambda, \psi)$ space where $k_z$ is independent of $\lambda$. We plot in Fig. 2e the value of $k_z$ for several values of angular dispersion $\beta$. When mirrors sandwich a layer of thickness $d$, resonances are established whenever $k_z$ is an integer multiple of $\pi/d$. Setting $\beta = 0$, we retrieve the case of collimated light incident on a planar layer at an external angle of incidence $\psi$. As $\beta$ increases, the constant-$k_z$ contours display less curvature with respect to $\lambda$. At $\beta = 0.37^\circ/\text{nm}$ we reach a critical condition where $k_z$ over an extended region in $(\lambda, \psi)$ space becomes independent of $\lambda$. A broadband optical beam prepared in this configuration will
transmit through an omni-resonant cavity via an achromatic resonance supported in this region. Increasing $\beta$ further reverses the curvature of the constant-$k_z$ contours with respect to $\lambda$, thereby disrupting the achromatic resonances.

**Experiment**

We have carried out an experiment to confirm this prediction of achromatic resonances utilizing a Fabry-Pérot cavity consisting of a 4-μm-thick layer of SiO$_2$ ($n = 1.48$ at $\lambda = 550$ nm) sandwiched between two Bragg mirrors each formed of 5 bilayers. Each bilayer comprises 92.2-nm and 65.5-nm-thick layers created by the evaporation of SiO$_2$ and Ti$_2$O$_3$ ($n = 2.09$ at $\lambda = 550$ nm), respectively, to produce a 120-nm-wide reflection band with $\approx 92\%$ reflectivity at its center wavelength $\lambda_c \approx 550$ nm at normal incidence. The cavity (total thickness $\approx 5.6$ μm) is deposited monolithically by electron-beam evaporation on a 0.5-mm-thick, 25-mm-diameter glass slide [Fig. 3b, inset]. Figure 3a depicts the measured spectral-angular transmission through the cavity obtained using a $\approx 3$-mm diameter collimated white-light beam from a halogen lamp revealing the standard behavior of a planar micro-cavity [25]. Upon normal incidence, a finite set of resonant wavelengths are transmitted with a FSR of $\approx 25$ nm, which are blue-shifted with angle of incidence $\theta$; see Supplement 1 for details.

We next modify the collimated white-light beam to produce the necessary condition to de-slant the resonance locus – without altering the cavity itself in any way. The beam is first spatially filtered through a 1-mm-wide vertical slit (to avoid aliasing of multiple resonance orders) and is then diffracted from a reflective grating with 1800 lines/mm [Fig. 3b]. The grating produces an angular dispersion of $\beta \approx 0.09^\circ$/nm at $\lambda_c = 550$ nm. A grating with $\approx 3500$ lines/mm produces the target $\beta$, but such a high-density grating has a low diffraction-efficiency in the visible. To enhance $\beta$, we add a lens in the path of the diffracted beam before the cavity [L1 in Fig. 3b]. The spectral transmission through the Fabry-Pérot cavity with tilt angle $\psi$ is plotted in Fig. 3c,d. It is critical to note that the angle $\psi$ is not the incidence angle of the beam onto the cavity, but is instead simply the tilt angle of the cavity with respect to the central wavelength $\lambda_c = 550$ nm that defines the optical axis (see Supplement 1); each wavelength is in fact incident at its own angle $\theta(\lambda)$. For convenience, we hold the grating fixed and rotate the cavity. Using L$_1$ with focal length $f = 50$ mm, $\beta$ is enhanced to $0.13^\circ$/nm, and the blue-shift of the resonance loci is boosted...
[Fig. 3c]. Reducing the focal length of L₁ to \( f = 25 \) mm increases \( \beta \) further and reaches the desired angular/spectral dispersion [corresponding to the third panel in Fig. 2e]. The resonance loci are now flattened horizontally at specific values of \( \psi \), whereupon all the wavelengths extending across a 60-nm-wide bandwidth – exceeding twice the FSR – resonate simultaneously [Fig. 3d], a phenomenon we name achromatic resonance.

As a result of the omni-resonant nature of the cavity, one may indeed image an object through it with broadband illumination. We add a lens to the setup in Fig. 3b to image a plane preceding the grating to a plane lying
Beyond the cavity (see Supplement 1). The object is a binary-valued $0.25 \times 2 \text{mm}^2$ transparency of the letter ‘i’ that is imaged through the cavity with a magnification factor of $\approx 3$. In absence of the grating, a limited amount of light is transmitted through the cavity at any incident angle due to the large FSR and narrow linewidth of the resonances lying within the cavity mirror bandgap [Fig. 4a,b]—when compared to the configuration where the cavity is absent [Fig. 4c]. In presence of the grating that renders the cavity transparent, a substantial amount of light is transmitted when the cavity tilt angle corresponds to that of an achromatic resonance at $\psi = 30^\circ$, $39^\circ$, $48^\circ$, and $57^\circ$ [Fig. 4a,d].

**Conclusion**

Our proof-of-principle experiment of an omni-resonant optical cavity renders transparent a micro-cavity with 0.7-nm-wide resonances separated by an FSR of $\approx 25$ nm, thanks to an achromatic resonance operating continuously over a broad spectrum ($\approx 60$ nm). Our approach is analogous to that of refs 19, 20, and relies on the same principle: coupling each spectral component of the input field to a particular spatial mode matching the resonance condition. In refs 19, 20 the set of spatial modes is discrete, whereas the set of spatial modes identified by the wave vectors in the planar cavities explored here spans a continuum.

Although the necessary correlation between wavelength and incidence angle is introduced using a planar surface grating, the bandwidth can be broadened further and the uniformity of the spectral transmission improved by replacing the grating with a metasurface realizing a customized function $\theta(\lambda)$ that takes into account the cavity mirror spectral phase $\gamma(\lambda, \theta)$, its polarization dependence, and wavelength dependence of the refractive index. Furthermore, such a metasurface may indeed implement the reverse-color sequence without introducing a tilt angle with respect to the cavity[27]. Consequently, depositing the metasurface directly on the planar micro-cavity may potentially result in ultra-thin optical devices that deliver resonant linear and nonlinear behavior over extended bandwidths.

We have introduced here a general principle that lifts the bandwidth restrictions associated with resonant linewidths in an optical micro-cavity—leading to the realization of an omni-resonant or white-light cavity. While recent work has exploited spectral splitting of the solar spectrum to optimize the photovoltaic conversion with multiple semiconductor junctions [28], our approach—on the other hand—implements a continuous mapping to a wavelength-dependent angle of incidence $\theta(\lambda)$. Indeed, our work extends to the continuum the correlations between discretized optical degrees of freedom studied in refs 29–31. As a result, the advantages associated with a resonance—such as field enhancement through resonant buildup and enhanced optical nonlinearities—become altogether decoupled from the cavity linewidth and are thus available over orders-of-magnitude larger bandwidths. This concept can have a profound impact on optics by bringing coherent perfect absorption to bear on harvesting solar energy, producing white-light micro-lasers, and yielding broadband resonantly enhanced nonlinear optical devices.

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Author Contributions
S.S. and A.F.A. developed the concepts and directed the research. S.S. performed the optical measurements and analysis. H.E.K. carried out simulations and prepared the figures. M.L.V. and J.D.P. designed the device. All authors analyzed the data. S.S., H.E.K., and A.F.A. wrote the paper with input from the co-authors.

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