Large linear magnetoelastic effect and field-induced ferromagnetism and ferroelectricity in DyCrO₄

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Abstract

All the magnetoelectric properties of scheelite-type DyCrO₄ are characterized by temperature- and field-dependent magnetization, specific heat, permittivity, electric polarization, and neutron diffraction measurements. Upon application of a magnetic field within ±3 T, the nonpolar collinear antiferromagnetic structure leads to a large linear magnetoelectric effect with a considerable coupling coefficient. An applied electric field can induce the converse linear magnetoelectric effect, realizing magnetic field control of ferroelectricity and electric field control of magnetism. Furthermore, a higher magnetic field (>3 T) can cause a metamagnetic transition from the initially collinear antiferromagnetic structure to a canted structure, generating a large ferromagnetic magnetization up to 7.0 μB f.u.⁻¹. Moreover, the new spin structure can break the space inversion symmetry, yielding ferroelectric polarization, which leads to coupling of ferromagnetism and ferroelectricity with a large ferromagnetic component.

Introduction

The linear magnetoelectric (ME) effect and multiferroicity enable control of polarization P (magnetization M) by a magnetic (electric) field, which is beneficial for applications in spintronic devices, nonvolatile memories, high-sensitivity magnetic field sensors, etc.⁶⁻⁷. In the linear ME effect, the induced electric polarization or magnetization is proportional to the applied magnetic field H or electric field E, which can be expressed as P = αH or μ₀M = αE, where α denotes the linear ME coefficient and μ₀ denotes the magnetic permeability of a vacuum. Since the first observation of the linear ME effect in Cr₂O₃ in the 1960s, the search for single-phase ME multiferroics with larger α values has attracted much attention. The maximum α obtained for a nonpolar antiferromagnetic (AFM) structure is <40 ps m⁻¹ usually.⁶ It is important to obtain a larger and constant ME effect in wider temperature and/or magnetic field regions for potential applications.

In the 1990s, the term “multiferroics” was proposed to describe materials that simultaneously exhibit more than one ferroic order, such as ferromagnetism, ferroelectricity, and ferroelasticity, in a single phase.¹⁰ Among the different multiferroics, the spin-ordering-induced ferroelectrics (i.e., ME multiferroics) attracted significant attention owing to the strong ME coupling. Based on the magnetic space group, collinear ferromagnetic (FM) spin alignment cannot break the spatial inversion symmetry. Therefore, electric polarization in single-phase ME multiferroics is often induced by some peculiar AFM or canted AFM spin structures instead of collinear ferromagnetism.¹⁶ Consequently, the magnetic moment is too small to be effectively controlled.¹⁷⁻¹⁹ It is very challenging to obtain a material with strongly coupled

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FM–ferroelectric properties and a considerable magnetic
moment.

DyCrO$_4$ has a rare Cr$^{5+}$ valence state. Under ambient
conditions, it crystallizes into a zircon-type crystal struc-
ture with the space group of $\text{I}_4_1$/amd$^{20,21}$. An FM phase
transition with a large magnetocaloric effect occurs at
approximately 23 K$^{22–24}$. Moreover, the zircon-type
structure is sensitive to external pressure. A pressure-
induced irreversible structural phase transition toward a
 scheelite-type new phase with $\text{I}_4_1$/a symmetry has already
been reported$^{25}$. In contrast to the FM zircon phase, the
 scheelite phase exhibits a long-range AFM transition$^{26–28}$. In
this study, scheelite-type DyCrO$_4$ was prepared in a
poly-crystalline form by a high-pressure and moderate-
temperature treatment method (see “Materials and
methods” below). Based on the powder X-ray diffraction
(XRD) and neutron diffraction results, there is no dis-
cernible impurity phase, such as the residual FM zircon
phase, or decomposed DyCrO$_4$ pervoskite phase (see
Supplementary Figs. S1 and S2 for details). This com-
 pound has a nonpolar collinear AFM ground state with
zero magnetic field. Within $\mu_0H = \pm 3$ T, a large and almost
constant linear ME effect is observed, enabling $H$ control
of $P$ and $E$ control of $M$. Under higher magnetic fields, a
metamagnetic transition occurs and is accompanied by a
large FM magnetization. Furthermore, the new spin
structure can break the spatial inversion symmetry and
thereby generate ferroelectric polarization. The presented
DyCrO$_4$ paves the way for novel investigations on
simultaneous direct and converse linear ME effects and
FM–ferroelectrics with large magnetic moments.

Materials and methods

Sample synthesis and XRD

To fabricate the scheelite-type DyCrO$_4$ sample, the
zircon-type sample was prepared at ambient pressure as a
precursor, as reported in a previous study$^{26}$. The prepared
zircon-type DyCrO$_4$ powders were pressed into a golden
cylinder with a diameter of 4.0 mm and height of 3.0 mm.
The cylinder was treated at 6–8 GPa and 700–750 K for
10–30 min on a cubic-anvil-type high-pressure apparatus
using pyrophyllite as a pressure transmission medium.
When the heating power was turned off, the pressure was
slowly released. The crystal quality and structure were
analyzed by powder XRD using a Huber diffractometer
with Cu $K_{\alpha1}$ radiation at 40 kV and 30 mA. The XRD data
were acquired at room temperature in the 2$\theta$ range of
10°–100° with steps of 0.005° and analyzed by Rietveld
refinement using the GSAS software$^{29}$.

Magnetic, specific heat, dielectric, and pyroelectric current
measurements

The magnetic susceptibility ($\chi$) and magnetization ($M$)
were measured using a magnetic property measurement
system (Quantum Design, MPMS-3). Both zero field-
cooling (FC) and FC modes were employed for $\chi$ mea-
surements at 0.01 T. The field-dependent $M$ measure-
ments were performed at different temperatures. The
specific heat ($C_p$) and electrical properties were measured
using a physical property measurement system (Quantum
Design, PPMS-9T). The $C_p$ data were acquired during
cooling in the range of 50–2 K with different magnetic
fields. For the measurements of the relative dielectric
constant $\varepsilon_r$, dielectric loss tan$\delta$, and pyroelectric current
density ($J$), the specimens were fabricated as thin plates
with a typical surface area of 1–2 mm$^2$ and a thickness of
0.2 mm. Silver electrodes were coated onto the two sur-
faces of the plate for electrical measurements. Different
frequencies of 1 kHz, 10 kHz, 0.1 MHz, and 1 MHz were
applied for the dielectric constant and dielectric loss
measurements at selected magnetic fields in the range of
0–9 T with intervals of 1 T using an Agilent E4980A
Precision LCR Meter while sweeping the temperature
from 2 to 50 K with a heating rate of 2 K min$^{-1}$. The
pyroelectric current was measured by a Keithley 6517B
precise electrometer while sweeping the temperature
from 2 to 50 K at a rate of 2 K min$^{-1}$. Before this meas-
urement, the sample was poled from 50 to 2 K with a
poling electric field of $E_{\text{pol}} = \pm 1.08$ MV m$^{-1}$. Once the
temperature was decreased to 2 K, $E_{\text{pol}}$ was switched off
and $J$ was measured as described above. The magnetic-
field-dependent current was measured while sweeping the
magnetic field at a rate of 0.01 T s$^{-1}$. In these measure-
ments, the PPMS was used to provide low-temperature and
magnetic field environments. The electric polarization ($P$) was
obtained by integrating $J$ as a function of
time. In addition, we measured the electric-field-induced
magnetization using MPMS-3 with different electric fields
produced by the Keithley 6517B electrometer. Before the
measurement, the sample was cooled from 50 to 10 K at a
rate of 2 K min$^{-1}$ at $E_{\text{pol}} = 0.5$ MV m$^{-1}$ and $\mu_0H = 4$ T.
Once the temperature was decreased to 10 K, both $E_{\text{pol}}$
and $H$ were switched off, and then $M$ was measured
during heating from 10 to 26.5 K at fixed temperatures and
selected electric fields.

Neutron diffraction measurements

The neutron powder diffraction (NPD) measurements
were carried out using the constant-wavelength high-
resolution neutron powder diffractometer HB2A at Oak
Ridge National Laboratory (ORNL). The temperature was
controlled by a Lakeshore Bridge, while the magnetic field
was generated by an Oxford-5 T superconducting magnet.
The temperature-dependent diffraction profiles were
measured at a wavelength of $\lambda = 2.41$ Å with the colli-
mation out-high intensity mode. The overall powder mass
was 1.3 g. To reduce the thickness to enable a neutron
transmission rate of approximately 90%, the sample
powders were spread out inside a 30 × 48 × 0.25 mm³ sample holder; their thickness was approximately 0.15 mm. The empty space in the sample holder was filled with Fluorinert to help fix the powders under a low temperature. The data were measured at different magnetic fields of 0, 1, 3, and 4.3 T. The magnetic refinements were carried out by the Rietveld method with the FullProf program

Results and discussion

As shown in Fig. 1a, the scheelite-type DyCrO₄ with a space group of I₄₁/a consists of spatially isolated CrO₄ tetrahedra and edge-sharing DyO₈ dimers. According to the space group, DyCrO₄ is centrosymmetric without spontaneous ferroelectric polarization in the crystal structure. With the decrease in temperature to \( T_N = 24 \) K, both the magnetic susceptibility measured at 0.01 T and specific heat at zero field show an AFM phase transition (Fig. 1b). Moreover, the NPD results at zero field (Fig. S2) suggest a collinear AFM spin structure composed of Dy\(^{3+}\) and Cr\(^{5+}\) spin sublattices, as presented in Fig. 1a. The magnetic symmetry analysis illustrates that the collinear AFM structure of DyCrO₄ has a magnetic point group of \( \Gamma_{\text{2m}} \), where the two-fold rotation is along the c axis, whereas the mirror is perpendicular to the c axis. This magnetic point group gives the ME tensor \( \alpha_{ME} \) with the form shown in Eq. (1). Therefore, although the magnetic group is nonpolar, it allows nonzero linear ME components, such as \( \alpha_{13}(\alpha_{31}) \) and \( \alpha_{23}(\alpha_{32}) \). This implies that an external \( H \) parallel to the c axis induces \( P \) along the a/b axis or vice versa while maintaining the initial spin structure, which can in principle lead to a linear ME effect.

\[
\alpha_{ME} = \begin{pmatrix} 0 & 0 & \alpha_{13} \\ 0 & 0 & \alpha_{23} \\ \alpha_{31} & \alpha_{32} & 0 \end{pmatrix}
\]  

To demonstrate the linear ME effect in an experiment, we first measure the temperature dependences of the relative dielectric permittivity and dielectric loss at different magnetic fields with an HLE configuration, as shown in Fig. 1c, d. At \( \mu_0H = 0 \) T, no anomaly in permittivity is observed in the measured temperature range. In contrast, a moderate magnetic field can induce an apparent dielectric peak near \( T_N \). Moreover, with the increase in the magnetic field, the dielectric peak becomes sharper and gradually shifts toward lower temperatures (Fig. 1c).

On the other hand, at a fixed \( H \), the dielectric peak is independent of the measurement frequency (Fig. S3). Analogous phenomena are observed in the dielectric loss with a maximum value <0.032 (Fig. 1d), indicating the intrinsic dielectric variations with the magnetic field. The dielectric measurements thus suggest \( H \)-induced \( P \).

To probe the off-diagonal nonzero components of the ME tensor \( \alpha_{ME} \) of the polycrystalline sample, we employ an ME annealing procedure with an HLE configuration, as described in the “Materials and methods” section and reported in the literature. In a polycrystalline sample with a random distribution of the grain orientation, such an ME annealing procedure can be used to choose one of the ME domains for each grain so that the macroscopic

![Fig. 1](image-url)

Fig. 1 a Crystal and antiferromagnetic spin structures of the scheelite-type DyCrO₄ at zero field. b Temperature dependences of the magnetic susceptibility and specific heat measured at 0.01 T and zero field. Temperature dependences of the c relative dielectric constant \( \varepsilon_r \) and d dielectric loss tan\( \delta \) measured at 1 MHz. Temperature dependences of the electric polarization after poling at different magnetic fields with e \( +E_{pol} \) and f \( -E_{pol} \).
ME effect can be observed considering the symmetry requirement. The temperature-dependent pyroelectric current was measured at the selected magnetic fields (Fig. S4), and then the related polarization was obtained by integrating the pyroelectric current as a function of the time. Using this approach, no significant $P$ is observed at $\mu_0H = 0$ T at temperatures down to 2 K, as shown in Fig. 1e. However, under an external $H\times E$ electric polarization is induced. The onset temperature of the induced $P$ is in close agreement with the position of the dielectric peak. Moreover, the sign of $H$-induced $P$ can be reversed by reversing the poling electric field $E_{\text{pol}}$ while maintaining the magnitude of $P$, as shown in Fig. 1f and Fig. S4. These results confirm $H$-induced polarization in accordance with the nonzero off-diagonal components in $a_{\text{ME}}$, which is expected from the AFM spin structure of DyCrO$_4$. Compared with the $H\times E$ configuration, the induced $P$ observed in our sample with an $H\parallel E$ configuration is considerably reduced (Fig. S5), consistent with the null value of the diagonal components of the ME tensor as presented in Eq. (1), although the detected $P$ is not exactly zero due to the polycrystalline nature of the sample.

As shown in Fig. 1e, $P$, at $\mu_0H \leq 3$ T, the magnitude of $H$-induced $P$ increases with $H$ and exhibits a broad maximum at approximately 15 K and then slightly decreases at lower temperatures. Moreover, if one looks at the pyroelectric current as presented in Fig. S4, the sign of the current measured at 2 and 3 T changes to be negative below approximately 15 K. This observation suggests that the Cr and Dy ions may have opposite contributions to the induced electric polarization $\sim H$. However, for $\mu_0H \geq 4$ T, the sign of the pyroelectric current is always positive. Correspondingly, the polarization gradually saturates and does not vary with further cooling. The essentially different polarization behaviors at lower and higher fields mentioned above are related to different spin structures due to a field-induced metamagnetic transition, as shown later. The maximum $P$ is observed in the range of 4−5 T, which may be attributed to the interaction between the Dy-$4f$ and Cr-$3d$ moments. Owing to the remarkable magnetic anisotropy, the applied magnetic field can change the magnetic state of Dy and thus affect the electric polarization. To elucidate the distinct polarization behaviors of these, we measured the magnetization as a function of the magnetic field at selected temperatures, as presented in Fig. 2a. Above $T_N$, $M$ exhibits a linear relationship with $H$ owing to paramagnetism. Below $T_N$, the linear magnetization behavior is also observed at lower fields owing to the collinear AFM ground state (see Fig. S6). However, with the increase in $H$ above a critical value ($H_c$), which is determined by the derivative of $M$ with respect to $H$, a metamagnetic transition occurs from the initial collinear AFM structure to a canted one. For example, at 2 K, the critical field is 3.1 T; a large magnetic moment up to $7.0\, \mu_\text{B}\, \text{f.u.}^{-1}$ caused by the metamagnetic transition is observed at field up to 7 T.

Further, the magnetic field-dependent dielectric constants were measured at selected temperatures (Fig. S7) to characterize the magnetodielectric (MD) effect (Fig. 2b). The MD curves display significant increases around $\mu_0H_c$ due to the metamagnetic transition, suggesting a different polarization behavior between the cases below and above $\mu_0H_c$. Moreover, the MD value at 20 K and 7 T reaches 11.4%, which is larger than the maximum MD value for the single-crystal multiferroic TbMnO$_3$.$^{11}$ The magnetic-field-dependent polarization was also measured to
distinguish the different ME features in DyCrO$_4$. Figure 2c, e show the resulting $P$ calculated from the corresponding ME current measurement results (Fig. S8) at 20 and 2 K, respectively. At 20 K, the polarization variation is close to linear within $\pm \mu_0 H_c$, reflecting the linear ME effect related to the collinear AFM; a sharp variation occurred around the critical field, above which the linear ME behavior was affected. The calculated linear ME coefficient $\alpha$ of DyCrO$_4$ at 20 K was approximately constant at 50 ps m$^{-1}$ in the region within $\pm \mu_0 H_c$ (Fig. 2d). Usually, the linear ME effects observed in collinear AFM materials without spontaneous electric polarization are quite small. For example, for a Cr$_2$O$_3$ single crystal, which is a prototype system for studies on the linear ME effect, the value of $\alpha$ is only approximately 2–4 ps m$^{-1}$\cite{33,34}. Co$_4$Nb$_2$O$_9$\cite{35} and LiCoPO$_4$\cite{36} exhibit larger linear ME effects, but the coupling coefficients are approximately 20–30 ps m$^{-1}$. Compared with those of most single-phase compounds with nonpolar collinear AFM spin structures, the $\alpha$ value for DyCrO$_4$ is one of the highest reported, even though our sample is polycrystalline. The TbPO$_4$ single crystal is an extraordinary example with an $\alpha$ value up to 730 ps m$^{-1}$ but only below a lower AFM transition temperature of 2.38 K.\textsuperscript{7} It is worth noting that a few ME multiferroics exhibit very large ME effects\textsuperscript{19,37–41}. However, they often only occur near the phase transition boundaries, while away from them, the ME effects are considerably reduced. In contrast, the ME coefficient of DyCrO$_4$ is relatively constant over the wide magnetic field range of $-\mu_0 H_c$ to $+\mu_0 H_c$. At low temperatures (e.g., 2 K) (Fig. 2e, f), the linear ME behavior of DyCrO$_4$ is also observed. At this temperature, the maximum $\alpha$ is increased to approximately 110 ps m$^{-1}$ at $\mu_0 H_c$. We will later discuss more about the different $P$–$H$ behaviors observed at 20 and 2 K.

In addition, we investigate the electric field-induced magnetization $M_E$, i.e., the so-called converse ME effect.\textsuperscript{7} Figure 3a shows the temperature dependence of $M_E$ measured in different electric fields. Below $T_S$, a considerable $E$-induced magnetization with magnitude tunable by the electric field is observed. Moreover, the sign of $M_E$ can be reversed upon application of an opposite measurement electric field. These features are very similar to those of the $H$-induced $P$, as shown in Fig. 1e, f. To further analyze the linear dependence of $M_E$ on the applied $E$, periodically varied electric fields (top panel in Fig. 3b) were used for $M_E$ measurements at 10 K and zero magnetic field. The middle and bottom panels in Fig. 3b present the obtained values of $M_E$ after ME cooling at $\mu_0 H = 4$ T and $E_{\text{pol}} = 0.5$ and $-0.5$ MV m$^{-1}$. The magnitude of $M_E$ periodically changes according to the periodic variation in the electric field. Furthermore, a linear relationship between $M_E$ and applied $E$ is observed, as demonstrated in the inset of Fig. 3b, confirming the converse linear ME effect of DyCrO$_4$. The converse ME coefficient derived from $dM_E/dE$ at 10 K is 26 ps m$^{-1}$, which is slightly smaller than the value obtained from the $H$-induced $P$ at 20 K.

The spin structure was studied in detail by NPD to investigate the spin origin of the electric polarization (see Supplementary Information for detailed analysis of NPD data). Figure 4a shows the net spin diffraction patterns obtained at 2 K under different magnetic fields after subtraction of the nuclear contribution from the collected NPD patterns (Fig. S2). At zero magnetic field, the spin structure composed of Cr$^{3+}$ and Dy$^{3+}$ was determined to be $k = (0, 0, 0)$ collinear AFM with spin moments parallel to the $a$ axis of the crystal lattice (Fig. 1a), agreeing well with a previous study\textsuperscript{28}. The refined magnetic moments of Cr$^{3+}$ and Dy$^{3+}$ at 2 K and 0 T are 1.0 ± 0.1 and 9.6 ± 0.5 $\mu_B$, respectively, as expected from the spin-only theoretical value for a 3d-Cr$^{3+}$ ion (1.0 $\mu_B$) and obtained

![Fig. 3 a] Temperature dependences of the induced magnetization magnetoelastic at selected electric fields for the scheelite-type DyCrO$_4$. b Prompt response of the magnetization to the regularly modulated electric field at 10 K. The top panel shows the modulated electric field, while the middle and bottom panels show the magnetizations polarized at 4 T with $E = 0.5$ MV m$^{-1}$ and $E = -0.5$ MV m$^{-1}$, respectively. $M$ as a linear function of $E$ is shown in the inset.
considering the orbital contribution for a $4f$-Dy$^{3+}$ ion (10.0 $\mu_B$). According to the symmetry analysis, the collinear AFM structure of DyCrO$_4$ has a nonpolar magnetic point group of $2/m$. The ME tensor of this magnetic group, as shown in Eq. (1), allows the generation of an intrinsic linear ME effect. Since both Cr$^{5+}$ and Dy$^{3+}$ take part in the AFM ordering and only a single anomaly is observed in magnetic susceptibility and specific heat curves (see Fig. 1b and Fig. S9), the Cr$^{5+}$ and Dy$^{3+}$ ions should order simultaneously at $T_N = 24$ K. We thus conclude that these two types of ions contribute to the large linear ME effect in DyCrO$_4$.

Upon the application of a magnetic field up to 4.3 T ($>\mu_0H_C$), the propagation vector remains unchanged $k = (0, 0, 0)$. The most notable variation is that the intensity of the magnetic (002) reflection gradually decreases with the increase in $H$ (Fig. 4a, b and Fig. S10). This change implies that the magnetic moments rotate toward the applied magnetic field, inducing canting of the collinear AFM structure, which yields a net FM moment. Considering the polycrystalline nature of the sample, it is difficult to exactly fit the magnetic peaks under a magnetic field, owing to the variable orientation of the magnetic field with respect to different magnetic domains. Constraining our analysis to the two existing magnetic states (i.e., collinear AFM structure determined at zero field and collinear FM structure with all of the moments parallel to a fixed axis such as the c axis), we can obtain the ratio between these two phases by fitting the scale factor while keeping the spin moments of Cr and Dy constant, as determined at 0 T. The results evaluated at 2 K are shown in Fig. 4c. The composition of the FM phase at 4.3 T is approximately $65 \pm 5\%$, indicating the strong ferromagnetism originating from the canted AFM alignment. After the metamagnetic phase transition above the critical magnetic field, the canted spin structure can be composed of both Dy$^{3+}$ and Cr$^{5+}$ spin sublattices (Fig. 4d) or just the dominant Dy$^{3+}$ sublattice (Fig. 4e). In these two cases, the magnetic point group always changes from the initially nonpolar $2/m$ to a polar $m$. This polar point group can break the space inversion symmetry and thereby cause spontaneous ferroelectric polarization, yielding field-induced ferromagnetism and ferroelectricity in the compound with strong coupling with each other. It is worth noting that magnetostriiction may occur under a high field, but this effect on the lattice change should be very small$^{42}$. Based on the above ME results, the presented DyCrO$_4$ is a rare material that simultaneously exhibits large direct and converse linear ME effects as well as field-induced ferromagnetism–ferroelectricity with a giant magnetic moment, making it distinct from other reported materials. For example, in the well-known type-II multiferroics such as TbMnO$_3$$^{11}$, the polarization originates from the spiral AFM ordering, and thus this structure does not exhibit a considerable net magnetic moment. Moreover, the converse ME effect is not observed in this compound because the magnetic field can easily change the spin structure. In compounds with (weak) ferromagnetism and electric polarization such as EuTiO$_3$ and GdFeO$_3$, although the polarization appears at a higher temperature (approximately 250 K in the EuTiO$_3$ thin film), the FM transition occurs at a significantly lower temperature (4.2 K in the EuTiO$_3$ thin film), indicating negligible ME coupling$^{43}$. In contrast to the field-induced polarization, in the weakly FM GdFeO$_3$, the magnetic field rapidly suppresses the polarization to zero at 2–3 T$^{44}$. 

Fig. 4 a Net spin diffraction patterns obtained at 2 K and different magnetic fields after subtraction of the nuclear contribution for the scheelite-type DyCrO$_4$. b Temperature dependences of the magnetic (002) peak at different magnetic fields. c Magnetic field dependence of the phase composition at $T = 2$ K. Schematic spin structures including the ferromagnetic components of d both Cr$^{5+}$ and Dy$^{3+}$ spin sublattices and e only Dy$^{3+}$ with $H$ along the c axis.
DyFeO$_3$ also has a field-induced ferroelectric state, but the accompanying magnetic moment is limited (<1.0 $\mu_B$ f.u.)$^{45}$.

Using the experimental data, a characteristic magnetic and electric phase diagram can be obtained for different temperatures and magnetic fields. As shown in Fig. 5, the solid circles ($T_c$) and triangles ($T_N$) represent the phase boundary between the spin/electric order and disorder for scheelite-type DyCrO$_4$. The values of $T_c$ are determined from the dielectric peaks shown in Fig. 1c, while $T_N$ is determined from specific heat data (Fig. S9). Below $T_N$ and $\mu_0H_c$, the compound has a nonpolar collinear AFM structure with a large linear ME effect. The $\alpha$ value of this phase is among the highest values for the single-phase ME materials with nonpolar collinear AFM structures. Moreover, the magnitude of $\alpha$ is almost constant in the wider magnetic field region of $-\mu_0H_c$ to $+\mu_0H_c$. In addition, the converse linear ME effect is also observed in this magnetic field region. Furthermore, the metamagnetic phase transition changes the nonpolar AFM spin structure to the polar structure with a large FM magnetization. A strong ferromagnetism coupled with ferroelectricity thus develops below $T_c$ and above $\mu_0H_c$. Note that, when the magnetic field increases to 9 T, the compound is located near the paramagnetic and paraelectric phases at 20 K, while the FM and ferroelectric phases set in at 2 K. This difference is the reason why $H$-induced $P$ at 20 and 2 K displays different behaviors in high magnetic fields, as shown in Fig. 2c, e. The presented DyCrO$_4$ is a rare material, which simultaneously displays large direct and converse linear ME effects in the nonpolar collinear AFM phase and field-induced ferromagnetism and ferroelectricity with a large magnetic moment.

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