Chromospheric backradiation in ultraviolet continua and Hα

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ABSTRACT

A recent paper states that ultraviolet backradiation from the solar transition region and upper chromosphere strongly affects the degree of ionization of minority stages at the top of the photosphere, i.e., in the temperature minimum of the one-dimensional static model atmospheres presented in that paper. We show that this claim is incompatible with observations and we demonstrate that the pertinent ionization balances are instead dominated by outward photospheric radiation, as in older static models. We then analyze the formation of Hα in the above model and show that it has significant backradiation across the opacity gap by which Hα differs from other strong scattering lines.

Key words. Sun: photosphere – Sun: chromosphere – Sun: UV radiation

1. Introduction

Static one-dimensional (1D) modeling of the solar atmosphere assumes hydrostatic equilibrium in plane-parallel-layer geometry to deliver temperature and density stratifications along vertical columns that may serve as reference description to compute spectral continua and lines similar to actual solar radiation. Early versions of such “standard” models were compiled by de Jager (1959) and Heintze et al. (1964a, 1964b), Holweger’s (1967) LTE best-fit to optical iron lines became the first choice in classical abundance determination, in particular as the HOLMUL update by Holweger & Müller (1974). This model describes only the photosphere and is close to theoretical photosphere models based on the additional assumption of energy conservation in the form of radiative equilibrium plus mixing-length convection in the deepest layers (e.g., Kurucz 1974, 1994; Gustafsson et al. (1975, 2008)). Semi-empirical best-fit modeling of solar continua including ultraviolet wavelengths sampling the chromosphere continued with the Bildtberg Continuum Atmosphere (Gingerich & de Jager 1968), the Harvard-Smithsonian Reference Atmosphere (Gingerich et al. 1971), the VAL model grids of Vernazza et al. (1973, 1975, 1981) fitting disk-center Lyman brightness bins, the update by Mathys et al. (1986), the more recent update concentrating on disk-center ultraviolet continua by Avrett & Loeser (2008), and the sequence of similar refinements by Fontenla et al. (1990, 1991, 1993, 2002, 2006, 2007, 2009).

This paper is triggered by the conclusion of Fontenla et al. (2009) that “in the solar chromosphere, the FUV and EUV observed emissions in continuum and lines produced in the lower chromosphere and transition region irradiate the low chromosphere and have significant effects on the ionization.”. In particular, they claim that such backradiation strongly affects the density of minority stages of ionization in and near the temperature minimum of their quiet-Sun model. We first show that this claim is incompatible with basic observations, and then use illustrative computations to demonstrate that, instead, photospheric irradiation from below is the dominant agent in ultraviolet continuum formation in the quiet-Sun model of Fontenla et al. (2009), as was the case for the older standard models.

We continue by demonstrating that significant chromospheric backradiation occurs in Hα in such static models through two-level scattering (Sect. 3), but argue that the assumption of columnar hydrostatic equilibrium is untenable for the chromosphere and transition region (Sect. 7).

2. Observation

In this section we briefly review the observational character of the chromosphere, as counterpart to the standard-model definition as the domain between the model’s temperature minimum and steep temperature rise towards the corona. Figure 1 gives an overview of the appearance of the solar atmosphere in an area containing plage and network. We use it to demonstrate that the actual chromosphere may have enough opacity to supply significant backradiation in Hα, but not in the 1700 Å continuum.

The G-band image and the magnetogram in the first column of Fig. 1 are photospheric. The first image displays the granulation and the spatial distribution of small kilogauss magnetic concentrations qualitatively and without sign through their proxy as intergranular bright points (best seen when zooming in). The second image quantifies the actual surface distribution of the line-of-sight component in such strong-field concentrations, but at lower angular resolution. The correspondence is excellent.
The other four images allegedly sample the chromosphere (1700 Å, Ca II H, Ha) and the transition region (He II 304 Å). However, only the Hα image truly shows the chromosphere. It consists of long slender fibrils that cover and obscure the photosphere everywhere in the form of overlying fibrilar canopies. This is always the case near active regions, plage, and active network; only the very quietest internetwork areas are not covered by fibrils in Hα (e.g., Plate 3.1 of Bray & Loughhead 1974; Rouppe van der Voort et al. 2007; Rutten et al. 2008). These ubiquitous Hα fibril canopies constitute the “chromosphere”. They are also likely to irradiate the low-opacity backradiation. Their geometry resembles that of the highly dynamic features seen as Ca II H α-fibrils (Reardon et al. 2009). Compared to the 1700 Å image, the Hα image is much like the 1700 Å image, apart from difference in angular resolution. In the internetwork scene is dominated by shock brightness in the inner line wings that swamps the signature of very dark fibrils at line center (Reardon et al. 2009). Compared to the 1700 Å image, there is an extra contribution from the form of a diffuse bright haze around network and plage that is likely the unresolved appearance of the highly dynamic features seen as Ca I H straws near the limb (Rutten 2008). Ca II H spicules-II outside the limb (De}

**Fig. 1.** Co-spatial simultaneous images from the Dutch Open Telescope (DOT) at [ftp://dotdb.strw.leidenuniv.nl](ftp://dotdb.strw.leidenuniv.nl) and from the Solar Dynamics Observatory (SDO) at http://lmsal.com/get_aia_data. First row: DOT images sampling the G band, the core of Ca II with 1.4 Å passband, the center of Hα with 0.25 Å passband. Second row: SDO/HMI magnetogram, SDO/AIA 1700 Å image, SDO/AIA He I 304 Å image. They were all taken on September 27, 2010 within a few seconds around 13:54:30 UT, a moment of excellent seeing at the DOT (Fried parameter r₀ ≈ 14 cm). The field of view (scales in arcsec, terrestrial North up) is near disk center, South of the largest sunspot of AR11109. It contains a ridge of plage in its upper half, quieter areas in its lower half. The grey scales have been optimized by clipping (all images) and logarithmic scaling (AIA images). We invite the reader to zoom in with a pdf viewer for better appreciation of the detail in the DOT images. DOT observer: E. Romashets. DOT speckle reconstruction: A. Sukhorukov. Alignment routines: P. Sütterlin.
The He II 304 Å image shows fibrilar patterns that are not identical to but also not unlike the Hα canopies. It also shows similar bright grains near fibril feet as Hα does. These are not cospatial with the bright grains in the G-band and Ca H images. The overall similarity suggests that hot transition-region gas shares the field-guided topography of the Hα chromosphere, outlining similar magnetic connectivity patterns. Such patterns seem also to be mapped by Lyα fibrils in VAULT images (Vouridas et al. 2010). Any fibril that is opaque in Hα must be very thick in Lyα but, comparably to Ca H, the cell-covering fibrils are very dark in Lyα whereas other structures, likely Doppler-shifted out of line-center obscuration, contribute larger brightness in the profile-summed V AULT images (Koza et al. 2009).

The conclusion from this section is that significant chromospheric backradiation may be expected in Hα and in He II 304 Å which show opaque fibrilar canopies that constitute the actual chromosphere. Ca H should show them too at line center, but the DOT image and all other H & K filtergrams have too wide a bandpass. In the 1700 Å image the absence of any fibrilar signature, bright or dark or as erasure of the internetwork pattern seen in such ultraviolet continua.

3. Formulation

Fontenla et al. (2009) based their claim of important chromospheric backradiation on their Fig. 4 containing graphs of population departure coefficients $b$ for selected levels of Si i, Si ii, Mg i, Mg II, Fe i, and Fe ii. Population departure coefficients measure the ratio of the actual population density (particles cm$^{-3}$) to the population computed assuming LTE. There are two formats differing in normalization. The first, called “Menzel” here, follows the original use by Menzel & Cilley (1937) who normalized hydrogen populations to the free proton density. The generalization is to use a partial Saha-Boltzmann evaluation to obtain normalization to the next ion stage (Eq. (6.3) of Jeffries 1968, Eqs. (13)–(15) of Vernazza et al. 1981). The other format, called “Zwaan” here, follows Wijbenga & Zwaan (1972) and uses the elemental abundance as normalization. The two conventions are 

$$b_i^{\text{Zwaan}} \equiv n_i / n_i^\text{LTE} \quad \text{and} \quad b_i^{\text{Menzel}} \equiv n_i / n_i^\text{LTE} / n_C / n_C^\text{LTE},$$

where $n_i$ is the population of level $i$, $n_C$ is the total population of the next ion, and the superscript LTE implies a complete solution of the Boltzmann-Saha LTE partitioning equations for the given level and all stages of the element. Sometimes the ion ground state $n_i$ is used instead of $n_C$ assuming $n_i \approx n_C$. When the atom or ion containing level $i$ is predominantly ionized, so that $n_C \approx n_C^\text{LTE}$ because most particles of the species are in the next-ion stage, then

$$b_i^{\text{Menzel}} \approx n_i / n_i^\text{LTE} \approx b_i^{\text{Zwaan}},$$

but when most of the element sits in level $i$ itself then

$$b_i^{\text{Menzel}} \approx n_i^\text{LTE} / n_C \approx 1 / b_C^{\text{Zwaan}}.$$
For Mg (1992) – hence the code’s name. We used the 66-level model atom for Mg I, using the multi-level accelerated lambda iteration method following Rybicki & Hummer (1991) – hence the code’s name. We used the 66-level model atom for Mg I of Carlsson et al. (1992) and a 12-level model atom for Mg II from Uitenbroek (1997). Mg II is represented by its ground state only. Other elements of which the more important transitions are explicitly evaluated in NLTE are H, Si, Al, and Fe. Partial redistribution is accounted for in Mg II h & k and Ly α and β. The violet and ultraviolet line haze (e.g., Greve & Zwaan 1984) causing a quasi-continuum is accounted for by sampling the 236 000 lines between λ = 1000 and 4000 Å in the extensive list of Kurucz (2001) every 20 mÅ, using a two-level coherent scattering approximation per wavelength in which the collisional transition probability of each sampled line is estimated from the radiative one with the approximation of van Regemorter (1962), rather than applying a common scattering recipe for all lines as done by Avrett & Loeser (2008). However, a test with the much simpler line-haze recipe of Bruls et al. (1992) showed only little differences with the results shown here.

Figure 3 shows the resulting NLTE and LTE ionization fractions for the Kurucz and FCHHT-B models. In both magnesium is virtually once-ionized throughout the atmosphere (below the transition region at h = 1900 km for FCHHT-B). Let us first interpret the simple LTE curves in the upper Kurucz panel, which reflect the competing effects in the Saha equation of the outward decreases of the temperature T and electron density N_e shown in the lower Kurucz panel. Both decreases are steepest in the deepest layers, where N_e drops from 10^{-1} to 10^{-4} of the hydrogen density N_H because hydrogen becomes neutral. The N_e/N_H ≈ 10^{-4} limit represents the combined abundance of the electron donor elements (Fe, Mg, Si, Al) and controls the H opacity. The steep T drop wins from the steep N_e drop so that the Mg I fraction increases and the Mg II fraction decreases with height. Around h = 500 km the N_e drop wins from the T drop so that the LTE Mg I fraction drops slightly. The outer exponential decay of this fraction follows the decreasing gas density (with constant N_e/N_H ≈ 10^{-4}) at constant temperature. The NLTE Mg I curve also shows near-exponential decay around h = 500 km, implying that the nonthermal contribution, from radiative instead of collisional ionization and recombination, is about constant with height.

The Mg I and Mg II curves in the FCHHT-B panel are closely the same as in the Kurucz panel up to the FCHHT-B temperature minimum at h = 800 km, just as the models are. Thus, up to this height magnesium ionization does not depend much on higher layers.

Figure 4 shows the population departures b of the magnesium ground states for the Kurucz and FCHHT-B models. Both b definitions are used (left and right columns). Mg II cannot be shown in the Menzel version because we do not include Mg II. Since most of the population per ionization stage resides in the ground state, these curves reflect the divergences between the LTE and NLTE ionization fractions in Fig. 3.

The FCHHT-B/Menzel curves in the last panel resemble the corresponding curves in Fig. 4 of Fontenla et al. (2002), which for Si II and Fe II dip yet deeper than for Mg II. At first sight the two deep dips in this panel would suggest large depletion of both Mg I and Mg II at the temperature minimum. However, for Mg II this dip is the reverse of the Mg II peak in the Zwaan panel following Eq. 8. In the Zwaan panels the Mg II curves remain near unity because even large overionization of Mg I and overpopulation of Mg II do not much affect the Mg II population, being dominant anyhow (Fig. 3).

Near and above the temperature minimum, the Mg I and Mg II curves in the first panel of Fig. 4 mimic the temperature structure of the model atmosphere, for Mg II reversely. This im-
sensitivity of the \( \mathbf{A} \) operator to the steepness of the \( S_j(\tau) \) gradient results in \( J > B \) where they uncouple. This excess produces a superthermal edge source function in the upper photosphere, with \( S = (b_i/b_i) B \) in the Wien limit for an edge between level \( i \) and ionization limit \( c \). Thus, the divergence between \( S_e \) and \( B_e \) for the edge at 1621.5 Å in Fig. 5 translates into the divergences between \( b_i \) (Mg ii) and \( b_1 \) (Mg i) in Fig. 4 that measure the source function departure from LTE for this edge. Similarly for \( b_i/b_i \) in the edge at 2512.4 Å (which is a more important ionization channel and continuum provider).

In a plane-parallel atmosphere \( J_e \) flattens out to a constant outer limit unless there is significant emissivity in higher layers. The 1D models have that in their transition regions where the steeply increasing temperature gives larger \( \epsilon \), causing renewed coupling to \( B_e \). Below the transition region, the flat \( J_e \) may cut through whatever the model specifies as chromospheric temperatures, so that the latter are mapped into the \( b_i/b_i \) ratio when \( S_e \) follows \( J_e \). In the FCHHT-B panel of Fig. 5 the 2512.4 Å edge shows such behavior. The 1621.5 Å edge has some \( S_e \) coupling to the higher chromospheric temperature and a yet smaller increase in \( J_e \), which rises slightly above the flattened-out limit value for the Kurucz model.

All this is beautifully illustrated across the VAL3-C spectrum in Fig. 36 of Vernazza et al. (1981) and is explained at length in Rutten (2003).

There is no significant difference between the two models in Fig. 5 at the heights of formation of these bound-free Mg i continuum contributions. For both edges the formation is purely photospheric. Backradiation from the upper chromosphere plays no role.

The conclusion from Figs. 3, 5 is that the FCHHT-B model differs quantitatively from VAL3-C, but not qualitatively and not in its radiation physics. In particular, the continuum formation at these ultraviolet wavelengths is identical between the two models used here since the differences in \( S_e \) at larger heights are not sampled by the photospheric contribution functions.

Figure 6 adds FCHHT-B \( b \) curves for selected excited levels in Mg i and Mg ii to the ground-state display in the upper panels of Fig. 4. The Mg i ground state has the largest NLTE deficit in the temperature minimum due to \( J > B \) overionization in the principal Mg i edges. The plateau of \( b_i \) (index 0) excess at larger height maps \( J < B \) in these scattering edges.

The higher levels in Mg i converge to the \( b = 1 \) value of the Mg ii ground state, with multi-level crossstalk (“interlocking”). In the Mg i Rydberg domain this convergence is maintained by a collisional population replenishment flow driven by photon losses in intermediate Mg i lines, exemplified by the deep onset of the drop in the \( n = 10 \) curve. Such photon-loss replenishment from the next-ion population reservoir was called photon suction by Bruls et al. (1992). The Rydberg flow causes the Mg i emission features near \( \lambda = 12 \mu \text{m} \) that were thought chromospheric by Zipin & Poppl (1989) but actually are photospheric (Carlsson et al. 1992).

The Mg ii \( b \) peaks in the second panel of Fig. 6 reflect the effect of \( J > B \) pumping in strong ultraviolet lines, similarly as in Fe ii (see Rutten 1988). A particular example of the latter is the weak Fe ii 3969.4 Å line between Ca ii H and H\( \epsilon \) discovered as limb emission line by Evershed (1929). Its on-disk emission was initially attributed to chromospheric backradiation by Lites (1974) but is actually caused by photospheric pumping in Fe ii resonance lines (Cram et al. 1980) which explains its extraordinary spatial intensity variation at the limb (Rutten & Stencel 1988).

Figure 5 illustrates this cause by plotting 100 Å-wide averages of \( S_e, B_e \) and \( J_e \) for the two major Mg i edges against height in the Kurucz and FCHHT-B models. The spectral averaging smooths the many superimposed line blends. These quantities are plotted as formal temperatures in order to combine them in single diagrams for the two wavelengths, removing the Planck function sensitivity to wavelength (which is exponential in the single diagrams for the two wavelengths, removing the Planck function from the Wien approximation valid here). Figure 5 shows that across the ultraviolet \( S_e \) tends to follow \( J_e \) at the heights where the radiation escapes (shown by the contribution functions at the bottom of the graphs), with \( J_e \approx B_e \) for the 2512 Å edge.

Single-transition scattering with \( S = (1 - \epsilon) J + \epsilon B \) is an excellent approximation for these edges which scatter strongly, with complete redistribution over the edge profile. The steep decrease of the collisional destruction probability \( \epsilon \) with height makes \( S \) uncouple from \( B \) already deep in the photosphere, at a thermalization depth much deeper than the radiation escape depth. The

5. Explanation

The behavior of \( \mathbf{b}_z \mathbf{w} \) (see Rutten 1988) is well-understood, in particular since the classic PhD analysis of the comparable iron spectrum by Lites (1972) (cf. Athay & Lites 1972; review by Rutten 1988). The deep dip results from the dominance of the radiation field \( J \) in the source function \( S \) of the Mg i ionization edges in the violet and ultraviolet, where the bar denotes opacity-weighted frequency averaging over the edge and \( J \) is the angle-averaged intensity over all directions.

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Figure 6. Population departures of selected magnesium levels in the FCHHT-B model. The level numbers increase with excitation energy. Left: Mg i. Right: Mg ii. Upper row: Zwaan definition. Lower row: Menzel definition.

1980.] Similar upper-photosphere \( \overline{T} > B \) pumping sets the \( b \) peak of the Mg m ground state in the first panel of Fig. 4.

The lower panels of Figure 6 repeat the \( b \) displays for the Menzel definition. The left-hand panels are the same, but on the right the Menzel panel shows reversals of the Zwaan panel due to the normalization by the Mg m population. It makes the Mg \( ii \) curves appear similar to the Mg \( i \) curves.

The lower panels of Figure 6 are similar to the corresponding Mg \( i \) and Mg \( ii \) panels in Fig. 4 of Fontenla et al. (2006). The look-alike sequences of dips, deepest for the lowest levels, in their six Menzel plots made by Fontenla et al. (2006) conclude: “All our results display overionization (i.e., ground-level departure from LTE coefficients smaller than unity) of all species around the temperature minimum. […] Also, near the temperature minimum the lower levels have smaller departure coefficients than the upper levels, indicating that the overionization of neutrals is a result from FUV and/or EUV irradiation which primarily affects lower levels. This indicates that overionization is much more affected by the irradiation from the upper chromosphere in continuum and emission lines than by the photospheric radiation and absorption lines. Therefore, we stress that the consideration of a realistic upper chromosphere is essential to the determination of the densities near the temperature minimum of (1) neutral low first-ionization-potential (FIP) elements, and (2) singly ionized high FIP elements. Even a very sophisticated calculation of the effects of lower chromospheric absorption lines on the elemental ionization can produce unrealistic results if it does not include upper chromosphere irradiation.”. This interpretation is incorrect. Downward irradiation does not affect the degree of ionization of these minority species around the temperature minimum of the FCHHT-B model. We have demonstrated this for Mg here; the same applies to Fe, Si, Al.

However, more positively, we wish to note that the modeling of Fontenla et al. (2006) is not impaired by this misinterpretation of its results, and that that does not detract value from their effort. In this era of giant computer programs it becomes non-trivial to diagnose what the output implies. Chromospheric physics is becoming a key area in solar research but does require understanding of complex non-equilibrium optically-thick spectrum formation. Our tutorial elucidation of this particular issue may be instructive to newcomers to the field.

6. Backradiation in H\( \alpha \)

Figure 7 shows formation parameters for H\( \alpha \) in the Kurucz and FCHHT-B models. It is similar to Fig. 8 in Zwaan et al. (2006) but here, prompted by the referee and in the vein of this paper, we add detailed analysis using the FCHHT-B model for demonstration. We do not regard it a viable explanation of actual solar H\( \alpha \) formation (Sect. 5), but use it rather as a one-dimensional didactic “FCHHT-B star”.

The left-hand panel of Fig. 7 illustrates H\( \alpha \) line formation in such a star without overlying chromosphere. At line center, \( J_r \) drops well below \( B_r \). This behavior differs from the \( J_r > B_r \) excesses of the ultraviolet continua in Fig. 4 because the Planck-function sensitivity to temperature is smaller at longer wavelengths, flattening the \( dB_r/\partial \lambda \) gradient, and because the substantial additional line opacity \( c' \) flattens the \( dB_r/\partial \nu \) (or \( c' \)) gradient yet more. The \( \lambda \) operator then produces \( J_r < S_r \) tending towards the \( S_r = \sqrt{S_B} \) surface value for a scattering isothermal atmosphere with constant \( \varepsilon \).

In the Kurucz model the H\( \alpha \) core originates from the upper photosphere around \( h = 400 \text{ km} \) as a deep, strongly scattering line with \( S_r \approx J_r \). The corresponding emergent profile is shown in the top panel of Fig. 8. It is well reproduced by applying the Eddington-Barbier approximation \( I_r \approx S_r (\tau_r = 1) \).

The righthand panel of Fig. 7 shows the formation of H\( \alpha \) in the FCHHT-B model. Its chromospheric high-temperature plateau supplies sufficient H\( \alpha \) opacity that at line center \( \tau_r = 1 \) is reached about a thousand km higher than in the Kurucz model. The line-center formation is again well described by \( I_r \approx S_r (\tau_r = 1) \approx J_r (\tau_r = 1) \), but the Eddington-Barbier approximation is less well applicable in the line wings which have a formation gap between photosphere and chromosphere (e.g., Schoolman 1972, Leenaarts et al. 2006). This gap is detailed in Fig. 9 which shows H\( \alpha \) opacities and optical depth scales, with the opacities multiplied by the scale height in the upper FCHHT-B photosphere (it doubles in the FCHHT-B chromosphere from a steep increase of the imposed non-gravitational acceleration). The line extinction has a deep dip in the temperature minimum. Correspondingly,
the optical depth buildup (dotted curves) levels out. At line center the FCHHT-B chromosphere has optical thickness $\tau_\nu = 3.5$. At $\Delta \lambda = -0.44$ \AA~$\tau_\nu = 0.3$ (outer tick) is reached already in the chromosphere but $\tau_\nu = 1$ only a thousand km deeper in the photosphere. At $\Delta \lambda = -0.74$ \AA~the FCHHT-B chromosphere is virtually transparent.

At line center the line extinction much exceeds the continuous extinction even in the dip, so that the total source function equals the line source function at all heights. In the wings the line extinction drops below the continuum extinction. Where this happens the total source function drops to the Planck function (not shown).

Figure 10 shows the departure coefficients $b_2$ and $b_1$ (Zwaan definition) governing Hα in the FCHHT-B model. The curve divergence $\log(b_1) - \log(b_2)$ corresponds to the curve divergence $\log(S_b) - \log(B_0)$ in the FCHHT-B panel of Fig. 7.

Throughout the near-isothermal FCHHT-B chromosphere the Hα opacity is nearly in LTE because the formation of Lyα is close to detailed balancing there. However, this is not the case in the deep temperature minimum and steep rise to the chromospheric temperature. Here the $\Lambda$ operator smooths the rapid temperature changes for the scattering-dominated Lyα source function (not shown) which has $S_\nu = T_\nu = B_\nu$. This Lyα smoothing causes the high peak in $b_2$ and considerable corresponding fill-in of the opacity dips in Fig. 9 illustrated for line center as difference with the much deeper dot-dashed LTE curve. In this manner Lyα scattering compensates for low-temperature Hα opacity loss when cool features are narrow in spatial extent. The $b_2$ peak in Fig. 10 doubles if CRD is adopted for Lyα, from additional smoothing through farther wing-photon travel.

The corresponding emergent intensity profile in the top panel of Fig. 8 is similar to the Kurucz result despite the disparate line formation. Both are reasonably good approximations to the observed mean quiet-Sun profile. Both gain fit quality in the wings if the computed continuum intensity is rescaled to the observed value. Increase of the microturbulence in the Kurucz model from 1.5 to about 10 km s$^{-1}$ produces a good core fit for this model as well.
The \( J \) curves in Fig. 7 show that the opacity gap in the FCHHT-B model contains much more H\( \alpha \) radiation than at corresponding heights in the Kurucz model. This H\( \alpha \) radiation fillsin causes a yet higher peak for \( b_3 \) in Fig. 10. It is detailed in the lower panels of Fig. 8. In the lower photosphere the H\( \alpha \) \( J \) profiles are the same for the two models, but above \( h \approx 250 \) km the Kurucz model gives absorption cores whereas the FCHHT-B model predicts slightly self-reversed cores across the opacity gap. This difference explains that for the Kurucz model \( S_{\nu} \) (shown by the line-center \( S \nu \) curve in the lefthand panel of Fig. 7) ends up higher than \( J \), at line center, whereas for the FCHHT-B model \( S_{\nu} \approx J_{\nu} \) coincides with line-center \( J \) across the opacity gap in the righthand panel of Fig. 7. The large core width of the highest-formed FCHHT-B profiles comes from large thermal broadening (about \( 10 \) km \( s^{-1} \)) and yet larger microturbulence (about \( 15 \) km \( s^{-1} \)).

Because the FCHHT-B chromosphere is near-isothermal the H\( \alpha \) formation is comparable to the classic results for a finite isothermal scattering atmosphere of \cite{AvrettHummer1965} in particular their optically thin but effectively thin case in which the line source function does not reach thermalization. The main difference is that the FCHHT-B chromosphere is irradiated from below. The impinging intensity profile in the outward direction is shown by the dotted curve in the bottom panel of Fig. 8. This line is much shallower than the emergent profile from the Kurucz model, in agreement with the much higher \( J \), above \( h \approx 200 \) km. A test with a hotter chromosphere, i.e., thicker in H\( \alpha \), gives more backradiation and a higher impinging profile with a bright self-reversed core. However, the deep emergent-intensity core remains about the same.

Thus, the presence of an opaque chromosphere changes the illumination profile with respect to the profile that emerges from the same photosphere without overlying chromosphere. A mathematical explanation is given by the principle of invariance (page 165 of Chandrasekhar1950) regarding addition or subtraction of a layer of arbitrary optical thickness to a semi-infinite parallel-parallel atmosphere; creating a gap or pushing down the finite chromospheric atmosphere over the gap to where it meets similar source conditions does not change the emergent radiation. A more physical explanation is that the radiation field in the gap builds up due to backradiation from the overlying atmosphere (called reflection by Chandrasekhar1950).

We now demonstrate that this backradiation is dominated by two-level scattering. The line source function for complete redistribution can be written as:

\[
S_{\nu} = (1 - \epsilon_{\nu 0} - \eta_{\nu 0}) J_{\nu 0} + \epsilon_{\nu 0} B_{\nu 0}(T) + \eta_{\nu 0} B_{\nu 0}(T_d) + \rightangle \frac{J_{\nu 0} + \epsilon_{\nu 0} B_{\nu 0}(T) + \eta_{\nu 0} B_{\nu 0}(T_d)}{1 + \epsilon_{\nu 0} + \eta_{\nu 0}} \equiv \rightangle \frac{J_{\nu 0} + \epsilon_{\nu 0} B_{\nu 0}(T) + \eta_{\nu 0} B_{\nu 0}(T_d)}{1 + \epsilon_{\nu 0} + \eta_{\nu 0}} \equiv S_{\nu} \rightangle \frac{J_{\nu 0} + \epsilon_{\nu 0} B_{\nu 0}(T) + \eta_{\nu 0} B_{\nu 0}(T_d)}{1 + \epsilon_{\nu 0} + \eta_{\nu 0}} \rightangle \frac{J_{\nu 0} + \epsilon_{\nu 0} B_{\nu 0}(T) + \eta_{\nu 0} B_{\nu 0}(T_d)}{1 + \epsilon_{\nu 0} + \eta_{\nu 0}}, \tag{5}
\]

where \( S_{\nu} \rightangle \) is the profile-averaged mean intensity, \( \epsilon_{\nu 0} \rightangle \) the thermal destruction probability, i.e., the fraction of line-photon extinctions by direct collisional deexcitation corrected for emissivity from spontaneous scattering, \( \eta_{\nu 0} \rightangle \) the fractional probability of all indirect detour extinction, with detour meaning any multi-level path from the upper to the lower level not including the direct transition, corrected for stimulated detour emissivity, and \( \epsilon_{\nu 0} \rightangle \) and \( \eta_{\nu 0} \rightangle \) the corresponding ratios of such extinctions to the contribution by two-level scattering. The formal detour excitation temperature \( T_d \) is given by \( (g_v D_v)/(g_l D_l) \equiv \exp(h\nu_0/kT_d) \) where \( D_d \equiv \) the summed transition probability (per second per particle in the upper level) of all detour upper-to-lower paths, \( D_l \) for all detour lower-to-upper paths, and \( g_l \) and \( g_v \) are the statistical weights.

The classic literature used Eq. 5 (e.g., Gebbie & Steinitz1974, Sect. 8.1 of Jeffries1968, Eq. 12.11 of Mihalas1970, following Thomas1957 who divided strong lines into “collision type” with \( \epsilon_0 \rightangle \eta_0 \) and “photoelectric type” with \( \eta_0 \rightangle \epsilon_0 \), designating H\( \alpha \) as principal example of the second type. In particular, H\( \alpha \) would gain most photons from Balmer ionization followed by a recombination path into \( n = 3 \) employing photospheric Balmer photons (e.g., Athay & Thomas1961; see also Cram1985). The corresponding schematic source function diagram in Fig. 3 of Jeffries & Thomas1959 (reprinted in Fig. 12-9 of Mihalas1970 and Fig. 11-11 of Mihalas1978) is qualitatively similar to the FCHHT-B H\( \alpha \) behavior in Fig. 7 with \( S_{\nu} \rightangle \) leveling out in the photosphere to become much higher than \( B_{\nu 0} \rightangle \) in the temperature minimum.

However, in the FCHHT-B case this behavior is due to the backscattering from the chromosphere, not from Balmer-continuum detour emission. If the latter were important it would raise the H\( \alpha \) source function also for the Kurucz model. The Balmer continuum scatters outward similarly to the 2512 \( \AA \) continuum in Fig. 5 the same in both models up to \( h \approx 800 \) km, with about 1400 K radiation temperature excess in the temperature minimum – but that region is transparent in H\( \alpha \).
The scattering nature of the Hα source function is demonstrated in Fig. 11 by comparing it with the mean radiation $T_{\nu 0}$ and the two-level approximation. They are closely the same everywhere. The differences are magnified in Fig. 12 showing the fractional collision and detour contributions. The collisional contribution is negligible except in the deep photosphere where collisional excitations create most Hα photons (with $\epsilon_{\alpha 0} \approx 1$ and $T_{\nu 0} \approx B_{\nu 0}$). The latter resonance-scatter outward. Higher up, the detour contribution is much larger, confirming the $\eta_{\nu 0}/\epsilon_{\nu 0}$ evaluation of Al et al. (2004) but still amounts to only a few percent of the line source function and raises the line-center intensity by only one percent of the continuum intensity. In the steep temperature rise of the FCHHT-B transition region the detour contribution grows rapidly to nearly 100%, but at negligible Hα opacity and therefore of no importance to the emerging profile – and not due to photospheric irradiation.

The conclusion from this section is that in the FCHHT-B model Hα is first and foremost a scattering line, with chromospheric backscattering boosting the line-center radiation across the opacity gap between photosphere and chromosphere. The Hα core emerges from the FCHHT-B photosphere but most photons were created in the deep photosphere. For Hα the FCHHT-B chromosphere is primarily a scattering attenuator that builds up its own irradiation from below. The main source function difference with other strong scattering lines such as the Ca ii resonance lines and infrared triplet is the effect of the opacity gap, not the amount of detour contribution.

7. Discussion

Static 1D modeling of the continua from the solar atmosphere has reached such sophistication that even the modelers themselves may misinterpret their results (Sect. 5). Interpretation of chromospheric fine structure using strong lines, in particular Hα, has relied more on cloud modeling (see the excellent review by Tziotziou 2007) than on static model-atmosphere interpretation as in Sect. 6. In the meantime, observations of the actual chromosphere (Sect. 2) have reached such spatial and temporal resolution that the worlds of the modelers and the observers now seem far apart. A third worldview is given by time-dependent numerical MHD simulations of the chromosphere (e.g., Schaffenberger et al. 2006; Lienaarts et al. 2007, 2010; Martinez-Sykora et al. 2011). Obviously, the different views should come together. It falls outside the scope of this paper to effectuate such synthesis, but we make a few salient points.

Emergent spectrum fitting. The FCHHT-B model and the AL-C7 model of Ayvett & Loeser (2008) fit the ultraviolet atlases about equally well, but differ appreciably in their stratifications (Fig. 3) and in their stratification physics. Both assume hydrostatic equilibrium, but the AL-C7 model gains additional chromospheric support from imposed turbulent pressure inspired by observed line broadening, as in its VAL and FAL predecessors. The FCHHT-B model gains chromospheric support instead from imposed non-gravitational acceleration inspired by the Farley-Buneman instability (Fontenla et al. 2008). Thus, best-fit model determination from such data does not represent a unique data inversion.

An extreme example of non-uniqueness is that the two disparate Hα formations in Fig. 7 with and without a chromosphere, can both fit the observed average Hα profile (top panel of Fig. 8). Figure 11 obviously suggests that chromospheric Hα formation as in the FCHHT-B model is more realistic than photospheric Hα formation as in the Kurucz model, but the predicted Hα profile cannot be used as discriminator.

One-dimensional continuum modeling. The similarity of the magnetogram, 1700 Å and Ca ii H panels in Fig. 11 suggests that 1D modeling along vertical columns which differs between internetwork, network, and plage may be a reasonable approximation for ultraviolet continua from these features. The bright grains that constitute network and plage mark strong-field structures that are roughly vertical. However, facular modeling towards the limb must then account for slanted viewing across such structures by cutting through different 1D models along the line of sight, as in the classic Zürich fluxtube modeling of e.g., Bünte et al. (1995).

Cloud modeling. The FCHHT-B chromosphere may be regarded as an horizontally extended isothermal slab but not as a constant-property cloud since it is more like a finite atmosphere, with density stratification, outward $S_\nu$ decay, and Eddington-Barbier-like Hα core formation. The source function is dominated by scattering (Fig. 11) and the slab is effectively thin (Fig. 11) so that the source function amplitude depends on the slab opacity. Due to backscattering, the Hα profile illuminating the slab from below (dotted curve in the bottom panel of Fig. 5) is shallower than for locations without an overlying chromospheric blanket (Kurucz prediction in the top panel of Fig. 5) and brightens for a thicker blanket. If actual fibrilar canopies share such properties than these upset classical cloud modeling.

At the suggestion of the referee, we added in the middle panel of Fig. 5 the outward intensity profile at that optical depth in the Kurucz model which equals the optical thickness of the FCHHT-B chromosphere. It is similar to the outward intensity profile impinging the latter (bottom panel) because the line formation is much more similar for the two models on optical depth scales than on geometrical height scales. The near-equality of these profiles suggests a new recipe for 1D Hα cloud modeling, namely to use the outward intensity profile in a radiative-equilibrium photosphere at optical depth equal to the cloud’s thickness as impinging background profile.

Dynamics. The actual internetwork atmosphere above the photosphere (in our view consisting of a cool clathroposphere, chromospheric fibril canopy, and a similar-morphology sheath-like transition region) is continuously shocked. In Hα ubiquitous internetwork shocks are evident in Doppler timeslices (e.g., Rutten et al. 2008; Cauzzi et al. 2009). In magnetic concentrations shocks are ubiquitous already in the photosphere. Shocks also produce the dynamic fibrils jutting out from network (Hansteen et al. 2006; De Pontieu et al. 2007). The elusive straws/spicules-H/REBs near network are even more dynamic. This basic chromospheric dynamism upsets static chromosphere modeling.

Departures from LTE. The FCHHT-B NLTE departures discussed here reach two to three orders of magnitude at the FCHHT-B temperature minimum (Figs. 3, 10) while the lower level of Hα is nearly in LTE where the line forms (Fig. 10). The non-equilibrium simulation of Lienaarts et al. (2007) predicts overpopulations of this level up to twelve orders of magnitude for cool post-shock phases, where the temperature may fall well.
below the temperature minima of the standard models (Leenaarts et al. 2011). Thus, dynamic behavior may dramatically increase the temperature variations and NLTE effects.

Height of the transition region. One-dimensional models for different features typically differ primarily in the height of their transition region. Simulations as the one of Leenaarts et al. (2007) suggest that the transition region above internetwork is kicked up and mass-loaded by field-guided flows that do not obey one-dimensional hydrostatic equilibrium. In this simulation the location of the transition region varies over \( h \approx 1000 - 4000 \text{km} \), with rapid changes, and is generally lower above magnetic concentrations. Such larger range than in the 1D model grids may better reflect actual variations in fibril-canopy height or corrugation.

\( \text{H} \alpha \) opacity gap. The \( \text{H} \alpha \) opacity gap and backscattering into it are properties of the FCHHT-B model. Do they also occur in the real Sun? The images in Fig. 1 roughly agree with FCHHT-B predictions: in the 1700 Å image no fibrils are seen whereas they appear opaque in the \( \text{H} \alpha \) image. Also, when one samples the real Sun in \( \text{H} \alpha \) away from line center (e.g., in DOT movies), the photospheric granulation appears when the fibrils become transparent, without an intermediate clapotisspheric scene as in the \( \text{Ca} \alpha \) and 1700 Å images in Fig. 1. Thus, a similar opacity gap seems to exist under the actual fibril canopies making up the internetwork chromosphere. The radiation crossing it, boosted by backscattering, will suffer substantial spatial smoothing of the photospheric scene. Some of it may leak out through an effectively thin fibril canopy, scatter around dark fibrils in photon channeling as suggested by Al et al. (2004) or be seen from aside as in the backradiation explanation of bright rims under filaments (e.g., Kostik & Orlova 1975, cf. Panasenco 2010).

\( \text{H} \alpha \) detour brightening. In the FCHHT-B model \( \text{H} \alpha \) is an almost pure scattering line (Fig. 1A). The detour contribution \( n_m(B_{\text{d}}(T_a) - n_0 I) \) to the line source function becomes important only in the transparent transition region (Fig. 1C). In the real Sun locations with very bright \( \text{H} \alpha \), such as the moss and active-region heart in Fig. 13 of Rutten (2007), may represent low-lying, denser transition regions that radiate \( \text{H} \alpha \) through recombination paths.

8. Conclusion

The development of standard models of the solar atmosphere, masteredmind by E.H. Avrett, represents a well-established pinnacle of sophistication with respect to the application of NLTE spectrum formation theory with the inclusion of numerous spectral features. However, the assumption of hydrostatic and time-independent equilibria without magnetism remains a far cry from the actual solar chromosphere, which is pervaded by shocks and rapidly changing magnetic fine structure in even the quietest regions.

Conversely, state-of-the-art magnetohydrodynamics simulations do a good job in emulating the small-scale magnetodynamics of the actual solar atmosphere, but they remain weak in properly treating non-equilibrium radiation. Implementation of the art of the 1D modelers into the 3D time-dependent codes of the simulators presents a formidable challenge, but seems the most promising venue to understand the enigmatic solar chromosphere (cf. Leenaarts et al. 2012).

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