Local excitations in mixed-valence bimetal chains

Shoji Yamamoto
Department of Physics, Okayama University, Tsushima, Okayama 700-8530, Japan
(Received 6 May 2002)

We investigate localized intragap states in mixed-valence bimetal chains in an attempt to encourage further explorations into quasi-one-dimensional halogen-bridged binuclear metal (MMX) complexes. Within a coupled electron-phonon model, soliton and polaron excitations in the two distinct ground states of MMX chains are numerically calculated and compared. Making a continuum-model analysis as well, we reveal their scaling properties with particular emphasis on the analogy between MMX chains and trans-polyacetylene.

PACS numbers: 71.45.Lr, 71.23.An, 71.38.-k

I. INTRODUCTION

Halogen (X)-bridged transition-metal (M) linear-chain complexes (MX chains) provide a fascinating stage performed by electron-electron correlation, electron-lattice interaction, low dimensionality and d-p hybridization. Representative materials such as Wolffram’s red (M = Pt, X = Cl) and Reihlen’s green (M = Pt, X = Br) salts possess mixed-valence ground states exhibiting intense and dichroic charge-transfer absorption, strong resonance enhancement of Raman spectra, and luminescence with large Stokes shift. When the platinum ions are replaced by nickel ones, monovalence Mott insulators are instead stabilized. Local states such as solitons and polarons, which can be photogenerated or induced by doping, are further topics of great interest lying in these materials. A large choice of metals, bridging halogens, ligand molecules, and counter ions enables us to investigate electron-phonon cooperative phenomena in the one-dimensional Peierls-Hubbard system systematically.

![Crystal structures of the pop complexes R₄[Pt₂(pop)₄X]·nH₂O (a) and the dta complexes M₂(dta)₄I (b) in the projection of the bc plane, where hydrogen atoms are omitted. The dotted lines represent hydrogen bonds in (a), while they correspond to van der Waals contacts in (b).](image-url)

FIG. 1. Crystal structures of the pop complexes R₄[Pt₂(pop)₄X]·nH₂O (a) and the dta complexes M₂(dta)₄I (b) in the projection of the bc plane, where hydrogen atoms are omitted. The dotted lines represent hydrogen bonds in (a), while they correspond to van der Waals contacts in (b).
In recent years, bimetallic metal analogs (MMX chains) have made our argument more and more exciting. They comprise two families: \( R_1[Pt_2(pop)_4X\cdot_nH_2O \ (X = \text{Cl, Br, I}; \ R = \text{Li, K, Cs}; \cdots ; \ \text{pop} = \text{diphosphonate} = \text{P}_2\text{O}_5\text{H}_2^{2-}) \quad [11] \) [Fig. 1(a)] and \( M_2(dta)_4I \ (M = \text{Pt, Ni}; \ dta = \text{dithioacetate} = \text{CH}_3\text{CS}^2_\text{−}) \quad [12,13] \) [Fig. 1(b)]. The pop complexes are in general semiconductors with charge-density-wave ground states of the conventional type \[14,15\] \[Fig. 2(a)] and \( M_2(bta)_4I \) \[Fig. 2(b)] follows around 80 K \[19\]. On the other hand, the dta-family platinum complex, \( \text{Pt}_2(dta)_4I \), exhibits metallic conduction at room temperature \[18\], which has never been realized in conventional MX compounds. With decreasing temperature, there occurs a metal-semiconductor transition at 300 K and further transition to a novel charge-ordering mode \[Fig. 2(b)] \ follows around 80 K \[19\].

The exciting observations have stimulated theoretical research. Carrying out quantum-chemical band calculations, Borslch et al. \[20\] attributed the novel valence distribution in \( \text{Pt}_2(dta)_4I \) to its structural distortion. Kuwabara and Yonemitsu \[21\] more extensively investigated the charge ordering and lattice modulation using various numerical tools. The author \[22\] also studied the ground-state properties with particular emphasis on the contrast between the dta and pop complexes. Quantum, thermal, and pressure-induced phase transitions were theoretically demonstrated \[23,24\] so as to interpret the observations, while the optical conductivity was calculated \[22\] in an attempt to evaluate the hopping amplitudes and Coulomb interactions.

Now we are led to take a step toward the excited states. Solitonic excitations are expected of doubly (or multiply in general) degenerate charge-density-wave systems. Ichinose \[26\] introduced the idea of domain walls into MX chains and Onodera \[27\] developed the argument pointing out some similarities between MX chains and the trans isomer of polyacetylene in the weak-coupling region. Baeriswyl and Bishop \[28\] extended the calculation to polaronic states laying emphasis on the strong-coupling region. Optical absorption spectra due to solitons and polarons \[29\] and their relaxation process \[30,31\] in MX chains were extensively investigated. Although photoexperiments on MX chains \[32\] are still in their early stage, the optical excitations must be a coming potential subject. Making full use of a simple but relevant electron-phonon model, we give a detailed description of intrinsic defects in MMX chains. Numerical calculations, together with an analytic argument in the weak-coupling region, reveal that MMX chains still exhibit a striking analogy with trans-polyacetylene in their excitation mechanism.

\[ \begin{align*}
\alpha_{n-1} &\quad b_{n-1} \\
M &\quad M \cdots \quad X \cdots \quad M &\quad M \cdots \quad X \cdots \quad M
\end{align*} \]

(a) Charge-density-wave (CDW)

\[ \begin{align*}
M^{2+} &\quad M^{2+} \cdots \quad X^{-} &\quad M^{2+} &\quad M^{2+} \quad X^{-} \cdots \quad M^{2+}
\end{align*} \]

(b) Alternate charge-polarization (ACP)

FIG. 2. Schematic representation of the two distinct ground states of MMX chains \[19\]: (a) Charge-density-wave (CDW) state whose X sublattice is dimerized; (b) Alternate charge-polarization (ACP) state whose \( M_2 \) sublattice is dimerized.

\[ \begin{align*}
\mathcal{H} &= -t_{\text{MX}} \sum_{n,s} (a_{n,s}^\dagger b_{n,s} + b_{n,s}^\dagger a_{n,s}) \\
&\quad - \sum_{n,s} [t_{\text{MXM}} - \alpha (t_{n+1}^{(a)} + t_{n}^{(b)})] (a_{n+1,s}^\dagger b_{n,s} + b_{n,s}^\dagger a_{n+1,s}) \\
&\quad - \beta \sum_{n,s} (t_{n}^{(a)} a_{n,s}^\dagger a_{n,s} + t_{n}^{(b)} b_{n,s}^\dagger b_{n,s}) \\
&\quad + \frac{K_{\text{MX}}}{2} \sum_{n} [\alpha (t_{n}^{(a)})^2 + (t_{n}^{(b)})^2]
\end{align*} \]
where $a^{\dagger}_{n,s}$ and $b^{\dagger}_{n,s}$ are the creation operators of an electron with spin $s = \pm$ (up and down) for the $M d_{z^2}$ orbitals in the $n$th $\text{MMX}$ unit. $t_{\text{MM}}$ and $t_{\text{MMX}}$ describe the intradimer and interdimer electron hoppings, respectively. $\alpha$ and $\beta$ are the intersite and intrasite electron-phonon coupling constants, respectively, with $K_{\text{MX}}$ being the metal-halogen spring constant. $t_n^{(a)} = v_n - u_{n-1}$ and $t_n^{(b)} = u_n - v_n$ with $u_n$ and $v_n$ being, respectively, the chain-direction displacements of the halogen and metal dimer in the $n$th $\text{MMX}$ unit from their equilibrium position. We assume, based on the thus-far reported experimental observations, that every $M_2$ moiety is not deformed. The notation is further explained in Fig. 2. We set $t_{\text{MM}}$ and $K$ both equal to unity in the following.

The Hamiltonian (2.4) convincingly describes the two distinct ground states of $\text{MMX}$ chains, which are schematically shown in Fig. 2. The CDW and ACP states are characterized by the alternating on-site electron affinities and interdimer transfer energies, respectively. Orbital hybridization mainly stays within each $M_2$ moiety in the valence-trapped CDW state, while it essentially extends over neighboring $M_2$ moieties in the valence-delocalized ACP state. Therefore, the CDW state is more stabilized by increasing $\beta$ and $t_{\text{MM}}$, whereas the ACP state by increasing $\alpha$ and $t_{\text{MMX}}$. The $M_2$ moieties are tightly locked together in the pop complexes owing to the hydrogen bonds between the ligands and counter cations, while they are rather movable in the dta complexes owing to the neutral chain structure. Thus a significantly larger $\alpha$ is expected for the dta complexes. In this context, Fig. 2 is well consistent with experimental observations: $\text{(NH}_4)_4\text{[Pt}_2\text{(pop)}_4\text{Cl}]$ exhibits a ground state of the CDW type [33], while $\text{Pt}_2\text{(dta)}_4\text{I}$ displays that of the ACP type [19]. In the weak-coupling region, $v_n = 0$ in CDW, whereas $u_n = 0$ in ACP. With increasing coupling constants, their arise mixed states with $u_n \neq 0$ and $v_n \neq 0$ [28,33,34]. We note that the present CDW and ACP are characterized as the lattice configurations $t_n^{(a)} = t_n^{(b)}$ and $t_n^{(a)} = -t_n^{(b)}$, respectively, regardless of each displacement $u_n$ and $v_n$.

### III. RESULTS AND DISCUSSION

#### A. Variational Treatment

We consider local excitations from these ground states. Under the constraint of the total chain length being unchanged, trial wave functions may be introduced as

$$t_n^{(a)} = \sigma t_n^{(b)} = (-1)^n l_0 \tanh[(n-a)\xi], \quad (3.1)$$

for solitons [35] and as

$$t_n^{(a)} = \sigma t_n^{(b)} = (-1)^n l_0 \{1 - \tanh(2\kappa d)\}
\times \left[\tanh(\kappa(n-a) + d) - \tanh(\kappa(n-a + d))\right], \quad (3.2)$$

for polarons [36,37], where $\sigma$ takes + and − on the CDW and ACP backgrounds, respectively, $a$ is the lattice constant, and $l_0$ is the metal-halogen bond-length change in the ground state. $x_0$ indicates the defect center in both functions, while $\xi$ and $\kappa^{-1}\tanh(2\kappa d)$ describe the spatial extents of solitons and polarons, respectively, all of which are variationally determined.

### B. Spatial Configuration and Energy Structure

We show in Fig. 3 the spatial configurations of the optimum defect solutions. Spin and charge are separate entities in the solitonic excitations, while the polaronic excitations exhibit the conventional spin-charge characteristics. Neutral solitons $S^0$ and polarons $P^\pm$ convey net spin densities $\pm \frac{1}{2}$, whereas no spin density accompanies charged solitons $S^\pm$. Their formation energies do not depend on their locations in the weak-coupling region, but the degeneracy is lifted with increasing coupling strength (Table I). As the Peierls gap increases, defects generally possess increasing energies and decreasing extents, and end up with immobile entities.

In order to investigate their electronic structures in more detail, we decompose the electron densities $a_n$ and $b_n$ into alternating $(\bar{a}_n, \tilde{b}_n)$ and net (nonalternating) $(\bar{a}_n, \tilde{b}_n)$ components as

$$a_n = \bar{a}_n + \tilde{a}_n; \quad \bar{a}_n = \frac{1}{2}(a_{n-1} + 2a_n + a_{n+1}),$$

$$b_n = \bar{b}_n + \tilde{b}_n; \quad \bar{b}_n = \frac{1}{2}(b_{n-1} + 2b_n + b_{n+1}), \quad (3.3)$$

and show them for positively charged solitons $S^+$ in Fig. 2. Now we can easily find out the positive charges accompanying the defects. One of the most interesting and important features of local excitations of this kind is their interfacial character. Let us define further the CDW and ACP order parameters using the alternating components as

$$O_n^{\text{CDW}} = (-1)^n \left(\bar{a}_n + \tilde{b}_n\right),$$

$$O_n^{\text{ACP}} = (-1)^n \left(\bar{a}_n + \tilde{b}_{n-1}\right), \quad (3.4)$$

which detect oscillations of the CDW and ACP types, respectively, and are also plotted in Fig. 2. We learn that
the CDW soliton reduces the CDW amplitude and induces the ACP amplitude instead in its center, while vice versa for the ACP soliton. Their trajectories are expressed as CDW $\rightarrow$ ACP $\rightarrow$ CDW and ACP $\rightarrow$ CDW $\rightarrow$ ACP, where $\overline{A}$ denotes the antiphase counterpart for the state A. Neutral solitons and polarons exhibit different types of interface, where certain kinds of spin-density-wave oscillation blend into CDW or ACP. Due to their mixed nature, solitons and polarons could be divided into more elementary defects in the vicinity of the phase boundaries.

Density of states for solitons and polarons are shown in Fig. 6. The four bands coming from the CDW background are, from the bottom to the top, largely made up of the bonding combination $\phi_+$ of binuclear Pt$^{2+}$-Pt$^{2+}$ units, that of Pt$^{3+}$-Pt$^{3+}$ units, the antibonding combination $\phi_-$ of Pt$^{2+}$-Pt$^{2+}$ units, and that of Pt$^{3+}$-Pt$^{3+}$ units. On the other hand, the major components of the four bands coming from the ACP background are $\phi_+$ orbitals of interdimer Pt$^{2+}$-X$^-\mathrm{Pt}^{2+}$ units, the $\phi_-$ orbitals of Pt$^{2+}$-X$^-\mathrm{Pt}^{2+}$ units, the $\phi_+$ orbitals of Pt$^{3+}$-X$^-\mathrm{Pt}^{3+}$ units, and the $\phi_-$ orbitals of Pt$^{3+}$-X$^-\mathrm{Pt}^{3+}$ units. Therefore, increasing $\beta$ splits both $\sigma$ and $\sigma^*$ orbitals in the CDW state, while in the ACP state the splitting between $\sigma$ and $\sigma^*$ orbitals is stressed as an effect of increasing $\beta$.
The soliton solutions commonly exhibit an additional level within the gap, whereas the polaron ones are accompanied by a couple of intragap levels. These levels are all found to be localized around the defect center. The level structures in the weak-coupling region suggest some similarities between small-gap \textit{MMX} chains and \textit{trans}-polyacetylene. However, in contrast with the case of polyacetylene \cite{35,37}, the level structure which is symmetric with respect to the middle of the gap breaks down with increasing electron-phonon interactions due to the lack of electron-hole symmetry. Besides the intragap levels, there appear a few related levels which are also localized around the defect center.

\textbf{C. Scaling Properties}

In order to illuminate the scaling properties of the solitons and polarons in more detail, we plot in Fig. 7 their characteristic lengths $\xi$ and $\kappa^{-1}\tanh(2\kappa d)$ as functions of the band gap $E_g$. Although we have calculated them with varying $\alpha$, $\beta$, and $x_0$, they are uniquely scaled by $E_g$ in the weak-coupling region as

$$\frac{\xi/a}{E_g^{0.98}}, \quad \frac{\tanh(2\kappa d)/\kappa a}{E_g^{1.03}}, \quad (3.5)$$

where the second decimal place varies with the data set taken into the fitting. It is convincing that such scaling laws break down as the defect extents come close to the length scale $a$. The formation energies are also scaled by the gap, as is shown in Fig. 8. In the weak-coupling region, the soliton and polaron energies are both degenerate with respect to their spin and location, and exhibit scaling formulae.
FIG. 8. The soliton and polaron formation energies averaged over $x_0$ as functions of the band gap $E_g$. The negatively (positively) charged solitons and polarons possess more (less) than three-quarter-filled electron bands and therefore their formation energies can not be defined in themselves. As for charged excitations, $E_S$ ($E_P$) is further averaged over $S^+$ ($P^+$) and $S^-$ ($P^-$).

$$E_S \sim 0.33E_g, \quad E_P \sim 0.46E_g.$$

With increasing gap, the degeneracy is lifted, where the CDW solitons have lower energies than their ACP counterparts at a given $E_g$, while vice versa for polarons. Now that we have obtained the numerical observations [24], we should be reminded of the defect states in trans-polyacetylene and a rigorous approach [37,38] to them.

Su, Schrieffer, and Heeger (SSH) [35] pioneeredly presented a theoretical study on the soliton excitations in polyacetylene. Although they employed a simple electron-phonon model, essential features of solitons such as the midgap localized energy level and the small effective mass were successfully interpreted. Takayama, Lin-Liu, and Maki (TLM) [36] mapped the SSH model onto a continuous line and obtained a rigorous soliton solution with the formation energy $E_S = E_g / \pi$. A polaron solution [36,37] was also found within the same scheme and its formation energy was revealed as $E_P = \sqrt{2E_g} / \pi$. Our numerical estimates [24], which are very close to the TLM findings, suggest that MMX chains still have an analogy with polyacetylene. Inquiring the continuum-model description of MMX chains, we try to understand the numerical calculations.

The continuum version of the present model (2.1) should be constructed from the primary $d_{\sigma^*}$ conduction band under no dimerization of the system. Without any electron-phonon coupling, the Hamiltonian (2.1) can be expressed as

$$\lim_{\alpha, \beta \to 0} H = \sum_{k,s} \left( \varepsilon_k^+ A_{k,s} A_{k,s} + \varepsilon_k^- B_{k,s} B_{k,s} \right),$$

where

$$\varepsilon_k^\pm = \pm \sqrt{t_{\text{MM}}^2 + t_{\text{MXM}}^2 + 2t_{\text{MM}}t_{\text{MXM}} \cos ka},$$

with $a_{k,s}$ ($b_{k,s}$) being the Fourier transform of $a_{n,s}$ ($b_{n,s}$) and

$$A_{k,s} = \frac{1}{\sqrt{2}} \left( e^{i\theta/2} a_{k,s} + e^{-i\theta/2} b_{k,s} \right),$$

$$B_{k,s} = \frac{1}{\sqrt{2}} \left( e^{i\theta/2} a_{k,s} - e^{-i\theta/2} b_{k,s} \right),$$

(3.9)

As far as we restrict our interest to the low-lying excitations, we may discard the irrelevant $d_{\sigma^*}$ band, which is here described by the dispersion relation $\varepsilon_k$, and linearize the relevant dispersion $\varepsilon_k^\pm$ at the two Fermi points. Taking account of the electron-phonon coupling within this scheme and assuming the CDW and ACP backgrounds, we obtain two effective Hamiltonians in the coordinate representation:

$$H_{\text{eff}}^{\text{CDW}} = t_{\text{eff}} \sum_{n,s} \left[ 1 - \frac{\Delta(na)}{t_{\text{MM}}} \right] (A_{n,s} A_{n+1,s} + \text{H.c.})$$

$$+ \frac{2t_{\text{eff}}}{t_{\text{MM}}} \sum_{n,s} \Delta(na) A_{n,s}^\dagger A_{n,s} + \frac{K_{\text{MX}}}{4t_{\text{eff}}^2} \sum_n \Delta(na)^2,$$

(3.11)

$$H_{\text{eff}}^{\text{ACP}} = t_{\text{eff}} \sum_{n,s} \left[ 1 - \frac{\Delta(na)}{t_{\text{MM}}} \right] (A_{n,s}^\dagger A_{n+1,s} + \text{H.c.})$$

$$+ \frac{2t_{\text{eff}}}{t_{\text{MM}}} \sum_{n,s} \Delta(na) A_{n,s}^\dagger A_{n,s} + \frac{K_{\text{MX}}}{16t_{\text{eff}}^2} \sum_n \Delta(na)^2,$$

(3.12)

where

$$t_{\text{eff}} = \frac{t_{\text{MM}}t_{\text{MXM}}}{2 \sqrt{t_{\text{MM}}^2 + t_{\text{MXM}}^2}},$$

(3.13)

$$\alpha_{\text{eff}} = \frac{1}{2} \left( \alpha + \frac{t_{\text{eff}}}{t_{\text{MM}}} \beta \right), \quad \beta_{\text{eff}} = \frac{t_{\text{eff}}}{t_{\text{MM}}} \beta,$$

(3.14)

$$\Delta(na) = \begin{cases} 2\beta_{\text{eff}}(-1)^{n}(u_n - v_n) & \text{for } H_{\text{eff}}^{\text{CDW}} \quad \text{and} \quad H_{\text{eff}}^{\text{ACP}}, \\
4\alpha_{\text{eff}}(-1)^{n}(u_n - v_n) & \text{for } H_{\text{eff}}^{\text{ACP}}, 
\end{cases}$$

(3.15)

In accordance with the slowly-varying gap parameter $\Delta(na)$, we introduce operators

$$\psi_{s}^{(r)}(na) = \frac{1}{\sqrt{L}} \sum_k e^{ika} A_{k+p+k,s},$$

$$\psi_{s}^{(l)}(na) = -\frac{i}{\sqrt{L}} \sum_k e^{ika} A_{-k-k+s},$$

(3.16)

for right- and left-moving electrons, respectively, where $L = Na, \ k_p = \pi/2a$ and $-\pi/2a < k < \pi/2a$. Now, summing out fast-varying components and taking the $a \to 0$ limit, we reach the relevant continuum models
Interestingly, when we rotate the spinor wave function around the z axis by the angle

\[
\varphi = \left\{ \begin{array}{ll}
\arctan(t_{MM}/t_{MXX}) & \text{for } \mathcal{H}_{CDW}^{\text{eff}}, \\
\arctan(t_{MXX}/t_{MM}) & \text{for } \mathcal{H}_{ACP}^{\text{eff}},
\end{array} \right.
\]

both Hamiltonians \((3.17)\) and \((3.18)\) turn into the same expression

\[
\mathcal{H}_{\text{TLM}} = \int \frac{\Delta(x)^2}{2\pi\hbar v_F \lambda} dx + \sum_s \int \Phi^d_s(x) \left[ -i\hbar v_F \sigma_z \frac{d}{dx} + \Delta(x) \sigma_x \right] \Phi_s(x) dx,
\]

which is nothing but the TLM continuum model. We know that the Hamiltonian \((3.22)\) possesses exact solitonic \([38,39]\) and polaronic \([36,37]\) solutions

\[
\Delta(x) = \Delta_0 \tanh(x/\xi), \quad E_S = 2\Delta_0/\pi,
\]

\[
\Delta(x) = \Delta_0 - \hbar v_F \kappa \\
\times \left[ \tanh \kappa(x + d) - \tanh \kappa(x - d) \right],
\]

with their characteristic scaling relations

\[
\xi = \hbar v_F/\Delta_0, \quad E_S = 2\Delta_0/\pi,
\]

\[
\tanh(2\kappa d)/\kappa = \hbar v_F/\Delta_0, \quad E_P = 2\sqrt{2}\Delta_0/\pi.
\]

Considering Eqs. \((3.13)\) and \((3.19)\) together with the relation \(2\Delta_0 = E_s\), we are fully convinced of the present numerical findings \((3.3)\) and \((3.6)\).

### D. Effective Mass

The continuum-model analysis has revealed that the defect extents should be given by \(2a/\sqrt{2}E_g\) in the weak-coupling limit under the present parametrization. According to the numerical observations \((3.5)\), this scaling law better holds for polarons than for solitons. This may be because polarons have wider extents than solitons at a given gap. When we consider moving defects, such an idea is quite suggestive. Let us calculate the effective masses of solitons and polarons.

Moving the defect center as \(x_0 = vt\) in Eqs. \((3.1)\) and \((3.2)\) and neglecting any change in the defect shape, which must be of order \(v^2\) due to the time-reversal symmetry and therefore does not contribute to the defect mass \(M_{\text{defect}}\) for small \(v\), we find

\[
\frac{1}{2}M_{\text{defect}}v^2 = \frac{1}{2}M \sum_n (j_n^{(a)})^2,
\]

where \(M\) corresponds to the mass of a halogen or bimetal complex according as the ground state is CDW or ACP. Assuming \(n\) to be sufficiently large under the periodic boundary condition, the summation in Eq. \((3.27)\) can explicitly be taken and ends up with

\[
M_S = \frac{4Ma^3}{3\xi} \left( \frac{l_0}{a} \right)^2,
\]

\[
M_P = \frac{8}{3} M \kappa a^2 \left( \frac{l_0}{a} \right)^2 \tan^2(2\kappa d) \\
\times \left[ 1 - 12(2\kappa d + 1 + (2\kappa d - 1) e^{2\kappa d})/e^{2\kappa d} - 3e^{2\kappa d} + 3e^{2\kappa d} - 1 \right].
\]
for solitons and polarons, respectively. Further calculation is performed for two well-studied MMX-chain materials \(K_4[Pt_2(pop)_2Br] \cdot 3H_2O\) with \(a = 8.139\ \text{Å}\) and \(Pt_2(dta)_4I\) with \(a = 8.633\ \text{Å}\). Their ground states were assigned to CDW and ACP, respectively, and therefore they give \(M = 145611me\) and \(M = 1375629me\), respectively, where \(me\) is the electron mass. We show in Fig. 4 that the calculated soliton and polaron masses, where the optimum values of \(\xi\), \(\kappa\), and \(d\) have been averaged over \(x_0\). For \(E_S \gtrsim 0.4\), any defect has to overcome site-dependent energy barriers in its motion and thus the present calculations are just for reference.

In comparison with the formation energy which describes a static defect and is generally given for both types of ground state in the weak-coupling region, the effective mass of a moving defect varies according to the background charge ordering. Defects on the ACP background generally look more massive than those of CDW counterparts. However, the difference should rather be attributed to the material-dependent crystalline structure than be recognized as a result of intrinsic defect features. CDW is accompanied by the halogen-sublattice dimerization, while ACP by the metal-sublattice dimerization. Larger defect masses on the ACP background reflect the mass of the diplatinum complex Pt\(_2\)(CH\(_3\)CS\(_2\))\(_4\) which is about ten times as heavy as the halogen atom Br.

On the other hand, the polaron mass turns out intrinsically smaller than the soliton mass. We have indeed found in Fig. 4 that the polarons are more spatially extended than the solitons at a given gap. The energy gap at least amounts to \(0.75\ \text{eV}\) in conventional MX-chain materials. Metal bimucletion strikingly reduces the gap, for example, to 0.08 eV for \(K_4[Pt_2(pop)_2Br] \cdot 3H_2O\) and 0.05 eV for \(Pt_2(dta)_4I\). Correspondingly, \(Pt_2(dta)_4I\) exhibits a high electrical conductivity 13 \(\Omega^{-1}\text{cm}^{-1}\), which is about 10\(^6\) times larger than that of a typical MX compound. Though we have no information on \(t_{\text{opt}}\), previous estimates of \(t_{\text{MXM}}\) for MX compounds \([3,4]\), together with the structural analyses \([10,12]\), imply that \(t_{\text{MXM}} = 1 \sim 2\) eV for MMX compounds. Then we are allowed to estimate that \(0.1me \lesssim M_S \lesssim 2me\) and \(0.05me \lesssim M_P \lesssim me\) for \(K_4[Pt_2(pop)_2Br] \cdot 3H_2O\), while \(0.3me \lesssim M_S \lesssim 3me\) and \(0.1me \lesssim M_P \lesssim me\) for \(Pt_2(dta)_4I\). In any case, the MMX-solitons are a few times as heavy as the MMX-polarons but still much lighter than the MX-solitons of \(M_S \gtrsim 100me\) \([27]\). There is a similar observation in trans-polyacetylene as well. The TLM-model analysis of polyacetylene gives \(M_S \simeq 3me\) and \(M_P \simeq me\) \([17]\). Such small masses should be quite significant in dynamics involving solitons and polarons. From the energetical point of view, we have learnt that \(E_P < 2E_S < 2E_P\). We can not well distinguish charged solitons from neutral ones within the electron-phonon model, but we find, taking account of electron-electron correlation, that \(E_S < E_{S\pm}\) \([18]\). Hence there may be a relaxation of photogenerated polaron pairs \(P^+ + P^- \rightarrow S^0 + S^0\) and a recombination of doping-induced or chemical-defect-associated solitons \(S^\pm + S^0 \rightarrow P^\pm\). In MX compounds, photogeneration of solitons and polarons have indeed been observed and they exhibit a varied relaxation process within a few hundred femtoseconds \([8,9]\). MMX chains with less massive defects may really exhibit picosecond dynamics.

IV. CONCLUDING REMARKS

We have investigated the local excitations corresponding to topological solitons and polarons in halogen-bridged diplatinum chains in terms of a coupled electron-phonon model. Although the solitons have lower excitation energies than the polarons, the effective masses of the solitons are larger than those of polarons. Their high mobility is promised in MMX chains with small energy gaps up to \(\sim 0.1\ \text{eV}\), where all the defects are at most a few times as massive as an electron.

There is an analogy between the defect states in MMX chains and those in trans-polyacetylene in spite of many contrasts between these systems such as \(d\) and \(\pi\) electrons, binuclear and mononuclear assemblies, and intrasite and intersite electron-phonon couplings. Then we are all the more eager to encourage optical measurements and doping of MMX chains, where the electronic gap is suitably small, chemical tuning of the electronic state is widely possible, and the single crystals are readily available.

ACKNOWLEDGMENTS

The author is grateful to A. R. Bishop, K. Yonemitsu, K. Nasu, and Y. Ono for fruitful discussions and helpful comments. This work was supported by the Japanese Ministry of Education, Science, and Culture and by the Sumitomo Foundation. The numerical calculation was done using the facility of the Supercomputer Center, Institute for Solid State Physics, University of Tokyo.

[1] R. J. H. Clark, in Advances in Infrared and Raman Spectroscopy, edited by R. J. H. Clark and R. E. Hester (Wiley, New York, 1984) Vol. II, p. 95.
[2] J. T. Gammel, A. Saxena, I. Batistić, A. R. Bishop, and S. R. Phillpot, Phys. Rev. B 45, 6408 (1992); S. W. Weber-Milbrodt, J. T. Gammel, A. R. Bishop, and E. Y. Loh, Jr., ibid. 45,6435 (1992).
[3] M. Tanaka, S. Kurita, Y. Okada, T. Kojima, and Y. Yamada, Chem. Phys. 96, 343 (1985).
[4] H. Toftlund and O. Simonsen, Inorg. Chem. 23, 4261 (1984).
TABLE I. The lowest- and highest-energy locations $x_0$ of MMX solitons and polarons.

| CDW background | ACP background |
|----------------|----------------|
| the lowest     | the highest    | the lowest     | the highest |
| $S^-$          | $(2n - \frac{1}{2})a$ | $(2n + \frac{1}{2})a$ | $(2n + 1)a$ | $2na$ |
| $S^+$          | $(2n + \frac{1}{2})a$ | $(2n - \frac{1}{2})a$ | $2na$ | $(2n + 1)a$ |
| $S^0$          | $(2n - \frac{1}{2})a$ | $(2n + \frac{1}{2})a$ | $(2n + 1)a$ | $2na$ |
| $P^-$          | $(2n + 1)a$ | $2na$ | $(2n + \frac{1}{2})a$ | $(2n - \frac{1}{2})a$ |
| $P^+$          | $2na$ | $(2n + 1)a$ | $(2n - \frac{1}{2})a$ | $(2n + \frac{1}{2})a$ |