A method based on circumferential strain distribution for roller path design in conventional spinning of thin-walled conical part with curved surface

Yongdi Wang · Hongwei Li · Pengfei Gao · Mei Zhan · Xinggang Yan · Haotong Niu

Received: 16 November 2021 / Accepted: 30 December 2021 / Published online: 12 January 2022
© The Author(s), under exclusive licence to Springer-Verlag London Ltd., part of Springer Nature 2022

Abstract
Multi-pass conventional spinning is the preferable forming technology for the forming of thin-walled conical part with curved surface (TCPCS) in aerospace field. In multi-pass conventional spinning, the design of roller path is a critical problem due to its sensitive effect on the deformation mode and forming defect during spinning process. However, at present, the roller path is still mainly designed based on experience and trial and error, which seriously restricts the high-performance spinning of TCPCS. In this work, a new quantitative method based on circumferential strain distribution was developed for the roller path design in multi-pass conventional spinning of TCPCS. In this method, the total required circumferential strain for the forming of final TCPCS by conventional spinning was firstly determined. Then, the spinning passes number was obtained through dividing the total required circumferential strain by the ultimate circumferential strain producing the spinning instability. As for the roller path profile in each pass, it is divided into two sections and determined, respectively, i.e., the attaching mandrel section and the preforming section. The attaching mandrel section presents the same profile of mandrel. The profile of preforming section is determined point by point by distributing the rest of circumferential strain to produce the final TCPCS. The point-by-point distributed circumferential strain is half of the total required circumferential strain in the initial stage until it reaches the half of the ultimate circumferential strain, and then, it will keep the half of the ultimate circumferential strain to the end. The proposed new method of roller path design was validated by finite element simulation, where well spinning stability, wall thickness distribution and roundness were obtained. This method provides a quantitative, high-efficient and universal way for the roller path design in conventional spinning of TCPCS.

Keywords Curved cone part · Conventional spinning · Roller path design · Circumferential strain distribution

1 Introduction
With the rapid development of aerospace and other high-tech industries, thin-walled complex parts with significant structural benefits are urgently needed in advanced aerospace equipment to reduce mass and improve overall performance [1]. Superalloy thin-walled conical part with curved surface (TCPCS) is such a typical component. However, due to the large deformation resistance of superalloy and the complex structure characteristics, it is necessary to select a reasonable forming process to achieve high-performance forming of these components. The possible forming processes of this kind of components generally include block welding, deep drawing and multi-pass conventional spinning. Compared with the former two forming processes, the multi-pass conventional spinning has the advantages of high precision, good performance, high material utilization, low cost, small forming force and high process flexibility, which is the most potential way to form these components [2, 3].

In the multi-pass conventional spinning process, the workpiece rotates along with the mandrel and the roller exerts local point loading along the specific roller path to produce the continuous local deformation, which gradually realize the integral forming of the component. It can be seen that the roller path is one of the most important parameters, which has crucial impact on the forming stability [4,
Some studies have shown that unreasonable roller path will lead to cracks, flange wrinkles and other defects [6, 7]. Because the roller path is a complex curve with high flexibility, its optimization design is very difficult [8]. In addition, the TCPCS usually has the characteristics of extreme size and special-shaped curved surface, which further increases the difficulty of the design of the roller path. Therefore, it is of great significance to study the design method of roller path for the multi-pass conventional spinning of TCPCS.

At present, some researches have been attempted on the influence of roller path on forming quality. Liu et al. [9] investigated the influence of straight line, arc and involute roller path on the distribution of equivalent stress and strain and found that the stress and strain were smaller under the involute roller path; Hayama et al. [10] found that compared with the straight and convex curve roller path, the spinning forming stability is the best and the flange is not easy to fluctuate under concave curve roller path. Wang and Long [11] studied the influences of concave–convex curve, concave curve, convex curve and straight line roller path on spinning forming force and wall thickness. It was shown that the spinning force of concave curve was the largest, while the convex curve roller path was beneficial to suppress the wall thickness reduction. James and Polyblank [12] selected B-spline curve as the spinning roller path to study the effects of four characteristic parameters of roller path profile on forming quality. The results indicated that the roller path with larger curvature is conducive to maintaining constant spinning force and the stability of flange state during spinning. The above studies have preliminarily studied the influence of single pass roller path on the forming results qualitatively, but not illustrated the design method of the total roller path in the whole spinning process.

In the aspect of roller path design for the spinning process, Chen et al. [13] proposed a design method of evenly spaced multi-pass involute roller path for the spinning process of cylindrical parts, while the base circle radius and the number of passes of involute path were given based on experience. Liu and Zhang [14] analyzed the multi-pass spinning process of the head with arc and straight generatrix. In their work, the involute roller path was used, whose design was given based on the establishment of the relationship between involute roller parameters and component diameter. However, the method of determined involute roller path is complex and lack of effectiveness verification. In view of the conventional spinning process of components with curved surface, the principle of circumferential strain uniform distribution between passes is proposed and proved by Guo et al. [15], which is beneficial to improve the forming accuracy and provides a theoretical basis for roller path design. However, the pass number and length of attaching mandrel path are determined by experience, and the influence of these two parameters on the forming quality is not specifically explored. In addition, the roller path profile is a specified type of concave curve and only considers the circumferential strain distribution between passes, while it ignores the circumferential strain distribution within the pass. Gao et al. [16] put forward a parametric roller path design method for curvilinear generatrix parts. Three different types of control point allocation for the spinning roller path are designed, which makes the roller path profile change. Huang et al. [17] proposed a asymptotic forming roller path generation method for general circular arc cross section parts, which means each pass is close to the component contour, and the attaching mandrel forming is not carried out until the last pass. It is easy to cause work hardening of material and reduce the wall thickness excessively for TCPCS. However, the method of roller path profile by dividing the circumferential strain of each point equally has important inspiration. To sum up, the above methods have some guidance for roller path design. However, in the above works, the roller path number and profile are strongly dependent on the experience and the certain type of curve, respectively, presenting limited universality. Therefore, it is needed to develop a new roller path design method with quantitative basis and independent of specific curve type.

The purpose of this paper is to propose a design method based on distribution of circumferential strain for roller path of conventional spinning. This method includes the determination of the number and position of spinning passes and the calculation of roller path profile. Then, the reliability of this method is verified. This method provides a quantitative, high-efficient and universal way for the roller path design in conventional spinning of TCPCS.

2 The design method for roller path

2.1 Geometrical feature of the conical part and roller path

As shown in Fig. 1, the contour line of the TCPCS is composed of four segments: 30° cone segment, R 500 arc segment, 18° cone segment and R 350 arc segment. The wall thickness is 0.8 mm. Because there is no change of half cone angle in 30° cone section, the shear spinning process can be used and the roller path is easy to get. The half cone angle of the remaining three sections decreases gradually to 10°. If the remaining three sections are formed by shear spinning, it is easy to cause excessive thinning, fracture and wrinkle due to large local deformation. Thus, the multi-pass conventional spinning is applied in the remaining three sections, which is helpful to solve above problems. For the multi-pass conventional spinning section, roller path is one of the key parameters, whose design method is focused in this study.
In this research, the design of roller path includes the determination of pass number \( n \), the profile and the position of each pass. The roller path in each pass is divided into the attaching mandrel section and the preforming section according to their different functions in the forming process. The attaching mandrel section is shown by the green line and the preforming section by the blue line, respectively. Subsequently, the design method for roller path will be described from two aspects: the determination of the number and position of spinning passes and the roller path profile.

### 2.2 Determination of the number and start position of spinning passes

The number of spinning passes is a key parameter in the roller path design. Too many passes will lead to excessive work hardening and thickness reduction. However, too few passes will cause instability in the spinning process. It is well known that wall thickness changes little in a pass of conventional spinning, which means the thickness strain can be ignored. Because the volume remains unchanged during deformation, the sum of circumferential strain and radial strain is zero. Circumferential strain plays great roles in the deformation during conventional spinning. Thus, the circumferential strain is used as deformation index for roller path design in this work. If the circumferential strain is too large during a spinning pass, the component is easy to wrinkle. Therefore, it is necessary to limit the circumferential strain. So, various linear roller paths with different circumferential strains were conducted to determine the ultimate circumferential strain \( \varepsilon_{\text{out}} \) by testing wrinkling degree. It is found that when the circumferential strain is no more than 0.025, there is no serious wrinkling of the blank. Thus, 0.025 is applied as the ultimate circumferential strain \( \varepsilon_{\text{out}} \) in this research.

In order to determine the number and start position of spinning passes, the required circumferential strain point by point in conventional spinning is needed to calculate. The premise of obtaining the circumferential strain point by point is to get the relationship between the points on the contour line of component and the corresponding points on the workpiece after shear spinning. As shown in Fig. 1, the axis of the mandrel is y-axis and the radius of the bottom perpendicular to the mandrel axis is regarded as the x-axis. To get the relationship between the points on the workpiece and the corresponding on the contour after forming, the contour and workpiece are discretized into microelements along the contour line and workpiece radius, respectively. The points on the contour line of component are represented by \( P(x, y) \), and the point set is \( \{ (x_0, y_0), (x_1, y_1), \ldots, (x_i, y_i), \ldots \} \). The corresponding points on the workpiece are represented by \( P'(x', y') \), and the set of points is \( \{ (x'_0, y'_0), (x'_1, y'_1), \ldots, (x'_i, y'_i), \ldots \} \), whose radial spacing is 0.5 mm. The coordinates of any two adjacent points are represented by \( P_{i-1}(x_{i-1}, y_{i-1}), P_i(x_i, y_i) \) and \( P_{i-1}(x_{i-1}, y_{i-1}), P'_i(x'_i, y'_i) \) at workpiece and the contour line, respectively, as shown in Fig. 2. Assuming that the thickness is constant \( t_0 = t \), where \( t_0 \) and \( t \) are the initial and deformed wall thickness, respectively in conventional spinning process, and combining with the volume invariance principle in plastic deformation, which means the volume of the ring before deformation is equal to that of the frustum ring after deformation, Eq. (1) can be obtained. Thus, the coordinates of any two adjacent points have the following relationship as shown in Eq. (2). Because the coordinates of the starting point are the same, Eq. (3) can be obtained.

![Fig. 1 Schematic of the geometry of TCPCS and roller path diagram](image1)

![Fig. 2 Schematic diagram of the relationship between the point on the workpiece and component](image2)
\[(x_i^2 - x_{i-1}^2) t_o \pi = \pi t \sqrt{(x_i - x_{i-1})^2 + (y_i - y_{i-1})^2} \times (x_i + x_{i-1}) \]

\[x_1' = \sqrt{(x_1 - x_{i-1})^2 + (y_i - y_{i-1})^2} \times (x_1 + x_{i-1}) + x_{i-1}^2 \]

\[x_0 = x_0', \ y_0 = y_0' \]

\[\theta_{1i} = \ln \frac{x_1}{x_i'} \]

Then, by substituting Eqs. (2) and (3) into Eq. (4), the circumferential strain at any point on the outline during the forming of final TCPCS from the workpiece after shear spinning is determined. The rest of circumferential strain is recorded as a set \(\{\varepsilon_{011}, \varepsilon_{012}, \ldots, \varepsilon_{01i}, \ldots\}\), in which the “1” in the second subscript represents the first pass, and the “i” in the third subscript indicates the i-th point. The distribution law of \(\{\varepsilon_{011}, \varepsilon_{012}, \ldots, \varepsilon_{01i}, \ldots\}\) is shown in Fig. 3a. It can be seen that, with the increase of X, the circumferential strain increases gradually. The maximum circumferential strain occurs at the larger diameter section of the component, which is the total circumferential strain required to complete the final forming of the component and recorded as \(\varepsilon_{01\text{max}}\).

The determination of spinning pass number \(n\) is based on the principle that making the circumferential strain of each pass is equal, and the value of circumferential strain is as large as possible, while it cannot exceed the ultimate circumferential strain. Therefore, when the circumferential strain of each pass is equal to the ultimate circumferential strain, the number of passes in the whole spinning process is the least. Thus, the number of passes is calculated by Eq. (5). According to Eq. (4), the maximum circumferential strain \(\varepsilon_{01\text{max}}\) is 0.3522, and the ultimate circumferential strain \(\varepsilon_{\text{ult}}\) is 0.025, so the number of passes \(n\) is 15.

\[n = \left\lfloor \frac{\varepsilon_{01\text{max}}}{\varepsilon_{\text{ult}}} \right\rfloor \]  

Partition the circumferential strain \(\{\varepsilon_{011}, \varepsilon_{012}, \ldots, \varepsilon_{01i}, \ldots\}\) in Fig. 3a with an interval of 0.025, the point of \(P_1\) to \(P_{15}\) can be determined as the positions of the entry points of 15 passes in x-axis. The intersections of the contour line and the vertical line are the position of the start point of each pass on the contour line, as indicated by point \(P_i'\) to \(P_{15}'\) in Fig. 3b. In addition, the length of attaching mandrel of each pass (the distance between the adjacent two start points in the contour line) can be achieved.

### 2.3 Determination of the roller path profile

The roller path profile is determined by calculating the position point by point based on a rule of circumferential strain distribution. As previously mentioned, the roller path in conventional spinning is composed of the attaching mandrel section and the preforming section, and the preforming section is further divided into the attaching mandrel section in next pass (AMSNP) and the non-attaching mandrel section in next pass (NMSNP). The profile of attaching mandrel section is designed according to the component contour, and the length of attaching mandrel section is described in Fig. 3b in Sect. 2.2. This section mainly introduces how to calculate the roller path profile of the preforming section based on the distribution of circumferential strain in each pass. The flowchart of calculation of roller path profile is shown in Fig. 4. In the first pass, there is only the preforming section. The rest of circumferential strain \(\{\varepsilon_{01i}\}\) to produce the final TCPCS is calculated point by point, and then, the roller path profile is determined by distributing the circumferential strain. Except for the first pass, the roller path profile of the remaining passes include the attaching mandrel section and the preforming section. Under this condition, the coordinate translation caused by the attaching mandrel section should
the deformation amount of the workpiece is $\alpha \varepsilon$ and the rest of circumferential strain $\varepsilon$.

At the beginning of the conventional spinning, the workpiece and roller path, the boundary condition can be shown in Eq. (7). Since there is the same starting point of the flat state to finished the first pass state, the expression of the final TCPCS is shown in Fig. 3a. The wall thickness can be derived as shown in Eq. (9). When $\alpha$ in Eq. (9) is determined, the first pass roller path profile can be obtained.

The roller path design method of other passes is same as the first pass except the calculation of $\{\varepsilon_{0ni}\}$. The detail procedure is as follows.

The roller path profile of the first pass preforming section is achieved by calculating the coordinates point by point under a principle of circumferential strain distribution. As shown in Fig. 5, the workpiece edges are a flat state at the beginning of the conventional spinning, and the rest of circumferential strain $\{\varepsilon_{0i1}\}$ to produce the final TCPCS is shown in Fig. 3a. The wall thickness is assumed to be constant during deformation ($t_0 = t$). Let the roller path coordinates set of the first pass be $\{(x_{10},y_{10}), (x_{11},y_{11}), \ldots, (x_{i1},y_{i1}), \ldots\}$, in which the “1” in the first subscript represents the first pass, and the “i” in the second subscript indicates the $i$-th point of the first pass. The corresponding point coordinates on the workpiece are $\{(x'_{10},y'_{10}), (x'_{11},y'_{11}), \ldots, (x'_{i1},y'_{i1}), \ldots\}$, whose radial spacing is 0.5 mm. Similar to 2.2, according to the principle of volume invariance during deformation, Eq. (6) can be achieved. The expression of $y_{i1}$ can be obtained as shown in Eq. (7). Since there is the same starting point of the workpiece and roller path, the boundary condition can be obtained as shown in Eq. (8). Based on Eq. (4) and assuming the deformation amount of the workpiece is $\alpha \{\varepsilon_{0i1}\}$ from flat state to finished the first pass state, the expression of $x_{i1}$ can be derived as shown in Eq. (9). When $\alpha$ in Eq. (9) is determined, the first pass roller path profile can be obtained.
The expression of the wall thickness is unchanged before and after deformation and can be obtained, where \( n \) is the number of passes. Taking the roller path design of the second pass as an example. In the spinning process, when the attaching mandrel section is completed in the second pass, the position of NMSNP in the first pass will move to yellow line as shown in Fig. 6. The \( \{e_{02i}\} \) represents the point-by-point circumferential strain generated in the process that the workpiece after finishing attaching mandrel in second pass is formed into final TCPCS. Thus, when we calculate the point-by-point \( \{e_{02i}\} \), the initial position of workpiece should be considered as the position of yellow line, which can be obtained by moving the position of NMSNP in the first pass. Similarly, the calculation of the rest circumferential strain \( \{e_{0ni}\} \) of the \( n \)-th pass need to consider the position change of the \((n-1)\)-th NMSNP after attaching mandrel in the \( n \)-th pass. Considering the above noteworthy points, the remaining steps for calculating the roller path profile of the second pass are calculated according to the method of first roller path profile and the details are as follows. The attaching mandrel section profile is same as the mandrel, and the clearance is 0.8 mm. For preforming section profile, when the second pass attaching mandrel is completed, let the preforming section of the second pass be described by the following points set \( \{(x_{20},y_{20}), (x_{21},y_{21}), (x_{22},y_{22}) \ldots \ldots (x_{2i},y_{2i}) \ldots \ldots \} \), and the coordinates of the corresponding in yellow line are represented by the points set: \( \{(x'_{20},y'_{20}), (x'_{21},y'_{21}), (x'_{22},y'_{22}) \ldots \ldots (x'_{2i},y'_{2i}) \ldots \ldots \} \). Similarly, it is assumed that the wall thickness is unchanged before and after deformation \( (t_2 = t_y) \). Eq. (10) can be obtained in any small deformation region depending on constant volume principle. The expression of \( y_{2i}, x_{2i} \), and the boundary condition are shown in Eqs. (11), (12), (13) and (14), respectively. The roller path coordinates are achieved by determining the \( \alpha e_{02i} \) value. The circumferential strain distribution rule is the same as that of the first pass. The roller path profile calculation method of the 3th-15th passes is the same as the second pass. According to the above steps, the designed 15 passes roller path is obtained based on circumferential strain distribution, as shown in Fig. 7, which is called simply as RPCSD.

\[
\pi t_2 \sqrt{(x_{2i} - x_{2(i-1)})^2 + (y_{2i} - y_{2(i-1)})^2 (x_{2i} + x_{2(i-1)})} = \pi t'_2,
\]

\[
\sqrt{(x'_{2i} - x'_{2(i-1)})^2 + (y'_{2i} - y'_{2(i-1)})^2 (x'_{2i} + x'_{2(i-1)})} = \pi t'_2.
\]

\[
A = \sqrt{(x'_{2i} - x'_{2(i-1)})^2 + (y'_{2i} - y'_{2(i-1)})^2 (x'_{2i} + x'_{2(i-1)})}
\]

\[
y_{2i} = \sqrt{\frac{A}{x_{2i} + x_{2(i-1)}}^2 - (x_{2i} - x_{2(i-1)})^2 + y_{2(i-1)}}
\]

\[
x_{2i} = e^{\alpha e_{02i}} + y_{2i}
\]

\[
x_{20} = x'_{20}, y_{20} = y'_{20}
\]

3 Verification of the designed roller path

The main purpose of this section is to prove the effectiveness of the roller path design method by simulating the spinning process of the superalloy TCPCS (Fig. 1). Therefore, it is necessary to establish a reliable spinning model [18]. Then, the simulation results under the designed roller path are analyzed to illustrate the effectiveness of the design method.
3.1 FE model for conventional spinning of TCPCS

The FE model for spinning of TCPCS is established by ABAQUS software. Considering the large deformation and complex contact conditions, the dynamic explicit algorithm is used. Figure 8a shows the assembly drawing of TCPCS spinning model, in which the material is GH3128 superalloy with thickness of 1.6 mm and diameter of 540 mm. The rollers and mandrel are defined as analytical rigid bodies, and the blank is deformation body. The material property parameters are selected according to the true stress–strain curve of GH3128 at 500 °C. The deformation behavior is described by Hollomon hardening criterion: \( \sigma = K \varepsilon^n \), and the specific material parameters are shown in Table 1. In order to simulate the spinning process more accurately, 4-node curved shell element S4R is adopted as the main element, as shown in Fig. 8b. Meanwhile, the 3-node triangular shell element S3 is used as the transition element. The size of element was controlled about one-fifth of the roller radius. The blank and the mandrel are fixed together by tie constraint to realize the rotation of blank under the drive of the mandrel. The Coulomb’s friction law is applied to simulate the contact behavior between the spinning tools and blank. The contact friction coefficient of two contact pairs including mandrel–blank and roller–blank is 0.02. The clearance between the contact point of the roller and the surface of the mandrel is 0.8 mm. In order to input the roller path, the coordinates of points on roller path were transformed relative to the reference point and decomposed on the x-axis and y-axis. Then, they are input in the boundary condition based on their relationship between coordinates and spinning time [19].

The reliability of the model is verified by comparing the shape and wall thickness distribution between simulation and experiment, the spinning roller path is composed of two sections, as shown in Fig. 8c. The shear spinning section is a 30° straight line, and the conventional spinning section is a concave curve. Based on experiments and literature research [7, 20, 21], the specific parameters of the experiment are shown in Table 2. The feed ratio of the shear spinning section and the conventional spinning section is 1 mm/s and 6 mm/s, respectively, and the spinning temperature is 500 °C. Finite element simulation and corresponding experiments were carried out with the above parameters.

Figure 9a compares the shape and dimensions between the simulated and experimental parts. It can be seen that their shapes are very similar with the relative errors of diameter and height being 0.53% and 1.32%, respectively. Taking four generatrices with an interval of 90° and calculating the average wall thickness at the same axial position, as shown in Fig. 9b, it can be found that the wall thickness distribution of the simulated and experimental parts presents a similar trend. The maximum thinning deviation and the average thinning deviation are 9.3% and 1.5%, respectively. The above analysis shows that the established finite element model is reliable.

| Material parameters                  | Values          |
|-------------------------------------|-----------------|
| Young’s modulus \( E \) (GPa)       | 169             |
| Poisson’s ration \( \nu \)          | 0.3             |
| Strength coefficient \( K \) (MPa)  | 1611.32         |
| Hardening exponent \( n \)          | 0.51            |
| Density \( \rho \) (g/cm³)          | 8.81            |

Fig. 8 Modeling description: (a) assembly drawing of TCPCS spinning model, (b) meshing diagram of blank and (c) spinning roller path.

and experiment under the same forming parameters. In the
3.2 Analysis of the forming result under designed roller path

Based on the effective spinning model, the designed roller path RPCSD is used to simulate the spinning process. The effectiveness of the RPCSD is confirmed by analyzing the stability of the deformation process, the uniformity of wall thickness and roundness.

Figure 10a, b shows the forming state after finishing the fifth and tenth pass, respectively. It can be discovered that the flange has no wrinkling phenomenon, which is benefit to conventional spinning. The RPCSD can make the component forming stability, and the final component is shown in Fig. 11a.

Figure 11a shows the simulation results using RPCSD. It can be seen that the wall thickness distributes within the range of 0.56–0.9 mm. The distribution of wall thickness along the generatrix is shown in Fig. 11b. It can be found that the wall thickness distribution is uniform and the average wall thickness is about 0.8 mm in the shear spinning section, which follows the sine law reduction. The wall thickness of conventional spinning section fluctuates in a certain range, while the standard deviation is only 0.0035 mm. The above analyses show that the wall thickness distribution is relatively uniform using RPCSD.

Roundness of spun parts is also an important quality index. Taking sections with an interval of 10 mm along the axial direction to measure, the ratio of the minimum radius to the maximum radius is calculated to evaluate the roundness. Figure 12 shows the distribution of roundness along the axial direction. It can be seen that the roundness decreases with the increase in axial distance, which means the roundness of workpiece gets worse a little. Thus, the roundness distribution is relatively uniform and well.

From the above analysis, it shows that the proposed design method for roller path in conventional spinning of TCPCS is effective. Moreover, this method has the following advantages: (1) It takes the deformation amount as the bridge to connect the roller path parameters and the geometry of the component together, which make the method has strong universality. (2) The roller path profile is obtained based on the distribution of the circumferential strain point by point, which does not depend on any type of curve.

![Image](image_url)

**Fig. 9** Comparison of simulated and experimental results: (a) shape dimensions; (b) wall thickness

| Table 2 Processing parameters in simulation and experiment |
|---------------------------------|-----------------|
| Basic parameters               | Value           |
| Diameter $D$ (mm)              | 540             |
| Thickness $t_0$ (mm)           | 1.6             |
| Spinning speed $N$ (r/min)     | 60              |
| Shear spinning feed rate $f_s$ (mm/s) | 1          |
| Conventional spinning feed rate $f_c$ (mm/s) | 6          |
| The angle between the axis mandrel and the axis of roller $\alpha$ (°) | 45              |
| Nose radius of roller $r_n$ (mm) | 10             |
| Diameter of roller $D_w$ (mm)  | 250             |
| Thickness of roller $H_w$ (mm) | 40              |
Conclusions

In this paper, a quantitative investigation was conducted on the roller path design in the multi-pass conventional spinning of thin-walled conical part with curved surface (TCPCS). The following conclusions can be drawn:

1. A new method based on circumferential strain distribution for the multi-pass roller path design for the conventional spinning of TCPCS was developed.

2. The method contains three important steps: (a) determination of the spinning passes number according to the ultimate circumferential strain producing the spinning instability ($\varepsilon_{\text{ult}}$); (b) determination the length and profile of the attaching mandrel section which takes the same profile of mandrel and extends to the point that whose circumferential strain reaches the $\varepsilon_{\text{ult}}$; (c) the profile
calculation of the preforming section through a point-by-point approach by distributing the rest of circumferential strain \(\varepsilon_{\theta ni}\) to produce the final TCPCS.

3. Case application in the conventional spinning of a superalloy TCPCS suggests that the proposed new method of roller path is effective and can obtain well spinning stability, wall thickness distribution and roundness. Different from the traditional empirical trial-and-error design method, this new method is a quantitative, high-efficient and universal way for the multi-pass roller path design in conventional spinning of TCPCS.

Acknowledgements This study is supported by National Natural Science Foundation of China (No. 92060107, No. U1737212) and National Major Science and Technology Projects of China (2019-VII-0014-0154).

Author contribution Yongdi Wang conceived the method and wrote the manuscript. Pengfei Gao directed and improved the method and put forward valuable suggestions for the writing of the article. Mei Zhan and Hongwei Li participated in article revision and provided project support. The contributions of Xinggang Yan and Haotong Niu lay in the discussion of previous methods and the inspection of manuscript, respectively. All authors discussed the results and commented on the manuscript.

Declarations

Ethical approval Not applicable.

Consent to participate Not applicable.

Consent for publication All authors have read and agreed to the published version of the manuscript.

Competing interests The authors declare no competing interests.

References

1. Lin YC, Deng J, Jiang YQ, Wen DX, Liu G (2014) Hot tensile deformation behaviors and fracture characteristics of a typical Ni-based superalloy. Mater Des 55:949–957. https://doi.org/10.1016/j.matdes.2013.10.071
2. Gao PF, Yan XG, Li FG, Zhan M, Ma F, Fu MW (2022) Deformation mode and wall thickness variation in conventional spinning of metal sheets. Int J Mach Tool Manuf 173:103846. https://doi.org/10.1016/j.ijmachtools.2021.103846
3. Gao P, Yu C, Fu M, Xing L, Zhan M, Guo J (2021) Formability enhancement in hot spinning of titanium alloy thin-walled tube via prediction and control of ductile fracture. Chinese J Aeronaut. https://doi.org/10.1016/j.cja.2021.01.002
4. Chen SW, Gao PF, Zhan M, Ma F, Zhang HR, Xu RQ (2019) Determination of formability considering wrinkling defect in first-pass conventional spinning with linear roller path. J Mater Process Tech 265:44–55. https://doi.org/10.1016/j.jmatprotec.2018.10.003
5. Wei ZC, Li WD, Wan M, Xu CX, Liu J (2010) Influence of roller trace on multi-pass conventional spinning process. J Plast Eng 17(3):108–112
6. Music O, Allwood JM, Kawai K (2010) A review of the mechanics of metal spinning. J Mater Process Tech 210:3–23. https://doi.org/10.1016/j.jmatprotec.2009.08.021
7. Xiao Y, Han Z, Zhou SY, Jia Z (2020) Experimental study of asymmetric multi-pass spinning. Int J Adv Manuf Technol 110:667–679. https://doi.org/10.1007/s00170-020-05913-7
8. Liu JH, Yang H (2003) Development of multi-process conventional spinning and research on roller-trace. Mech Sci Technol 22(5):805–807
9. Liu JH, Yang H, Li YQ (2002) A study of the stress and strain distributions of first-pass conventional spinning under different roller-traces. J Mater Process Tech 129:326–329. https://doi.org/10.1016/S0924-0136(02)00682-9
10. Hayama M, Kudo H, Shinokura T (2008) Study of the pass schedule in conventional simple spinning. Bull JSME 73:1358–1365. https://doi.org/10.1299/jsme1958.13.1358
11. Wang L, Long H (2011) A study of effects of roller path profiles on tool forces and part wall thickness variation in conventional metal spinning. J Mater Process Tech 211:2140–2151. https://doi.org/10.1016/j.jmatprotec.2011.07.013
12. James A, Polyblank JMA (2015) Parametric toolpath design in metal spinning. CIRP ANN-Manuf Technol 64(1):301–304. https://doi.org/10.1016/j.cirp.2015.04.077
13. Chen J, Wan M, Li WD (2008) Design of the involute trace of multi-pass conventional spinning and application in numerical simulation. J Plast Eng 015:53–57
14. Liu X, Zhang Y (1997) How to select the moving passes of the spinning roller. J Plast Eng 18:84–90
15. Guo H, Wang J, Lu G, Sang Z (2017) A study of multi-pass scheduling methods for die-less spinning. J Zhejiang Univ Sci A 18:413–429. https://doi.org/10.1631/jzus.A1600403
16. Gao L, Song J, Zhao Y, Yu Z (2021) Parametric roller path design in multi-pass conventional spinning of curvilinear generatrix parts. Int J Adv Manuf Technol 113:1637–1648. https://doi.org/10.1007/s00170-020-06556-4
17. Huang Y, Lu B, Chen J (2017) A parametric tool path design in multi-pass asymmetric spinning. J Eng Mater Technol 140:1328–1333
18. Wang L, Long H (2011) Investigation of material deformation in multi-pass conventional metal spinning. Mater Des 32:2891–2899. https://doi.org/10.1016/j.matdes.2010.12.021
19. Zhang J, Zhan M, Yang H, Jiang Z, Han D (2012) 3D-FE modeling for power spinning of large ellipsoidal heads with variable thicknesses. Comput Mater Sci 53:303–313. https://doi.org/10.1016/j.commatsci.2011.08.010
20. Wang L, Long H (2013) Roller path design by tool compensation in multi-pass conventional spinning. Mater Des 46:645–653. https://doi.org/10.1016/j.matdes.2012.10.048
21. Zhan M, Gao PF (2022) Conventional spinning of sheet metals for fabrication of metallic parts and structures 197–213. https://doi.org/10.1016/B978-0-12-819726-4.00019-3

Publisher's note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.