Metallothermic Reduction of MoO$_3$ on Combustion Synthesis of Molybdenum Silicides/MgAl$_2$O$_4$ Composites

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Abstract: Combustion synthesis involving metallothermic reduction of MoO$_3$ by dual reductants, Mg and Al, to enhance the reaction exothermicity was applied for the in situ production of Mo$_5$Si$_3$–, Mo$_5$Si$_3$– and Mo$_5$Al$_2$O$_4$ composites with a broad compositional range. Reduction of MoO$_3$ by Mg and Al is highly exothermic and produces MgO and Al$_2$O$_3$ as precursors of MgAl$_2$O$_4$. Molybdenum silicides are synthesized from the reactions of Si with both reduced and elemental Mo. Experimental evidence indicated that the reaction proceeded as self-propagating high-temperature synthesis (SHS) and the increase in silicide content weakened the exothermicity of the overall reaction, and therefore, lowered combustion front temperature and velocity. The XRD analysis indicated that Mo$_5$Si$_3$–, Mo$_5$Si$_3$– and Mo$_5$Si$_2$–MgAl$_2$O$_4$ composites were well produced with only trivial amounts of secondary silicides. Based on SEM and EDS examinations, the morphology of synthesized composites exhibited dense and connecting MgAl$_2$O$_4$ crystals and micro-sized silicide particles, which were distributed over or embedded in the large MgAl$_2$O$_4$ crystals.

Keywords: molybdenum silicides; MgAl$_2$O$_4$; aluminothermic; magnesiothermic; self-propagating high-temperature synthesis

1. Introduction

Molybdenum silicides, Mo$_5$Si, Mo$_5$Si$_3$ and MoSi$_2$, are promising intermetallic materials for ultrahigh-temperature structural applications. Besides a high melting point over 2020 °C, they possess high strength, excellent oxidation resistance, corrosion resistance, creep resistance and good compatibility with ceramic reinforcements [1–8]. To improve the refractory property of transition metal silicides, magnesium aluminate spinel (MgAl$_2$O$_4$) has been one of the potential additives, because of its unique combination of properties, including a high melting point (2135 °C), relatively low density, chemical inertness, high hardness, high mechanical strength and good thermal shock resistance [9–12]. However, preparation of MgAl$_2$O$_4$ via either wet chemical methods or solid-state reactions required several complicated steps under the long processing time [9–12].

As an alternative, metallothermic reduction reactions (MRRs) of metal oxides with Mg and Al as reducing agents produce MgO and Al$_2$O$_3$ as precursors for the formation of MgAl$_2$O$_4$ and such oxidation reactions are highly exothermic [13,14]. When combining Mg/Al-based MRRs with combustion synthesis, such a fabrication route is effective in producing MgAl$_2$O$_4$-containing composites. Moreover, the highly-exothermic MRRs render reduction-based combustion synthesis fit for self-propagating high-temperature synthesis (SHS). Many merits such as high energy efficiency, short reaction time, simplicity of operation and high-purity products have been recognized for the SHS process [15–17]. According to Horvitz and Gotman [18], reduction-based combustion synthesis using 2TiO$_2$–Mg–4Al samples was performed to produce TiAl–Ti$_3$Al–MgAl$_2$O$_4$ composites. Omran et al. [19] conducted co-reduction of WO$_3$ and B$_2$O$_3$ by Mg in the presence of Al$_2$O$_3$ to fabricate the composites of MgAl$_2$O$_4$–W–W$_2$B. By means of adopting pre-added MgO, Zaki et al. [20] obtained MgAl$_2$O$_4$ composites with MoSi$_2$ and Mo$_5$Si$_3$ from co-reduction of SiO$_2$ and...
MoO₃ by Al in argon at a pressure of 5 MPa. The high Ar pressure was to suppress the volatilization of MoO₃. Recently, Radishevskaya et al. [21] synthesized MgAl₂O₄ by the SHS method using the reactant mixtures consisting of MgO and Al₂O₃, along with Al as the fuel, Mg(NO₃)₂·H₂O as the oxidizer, and NaCl as the mineralizer. Results indicated that NaCl of 1 wt.% contributed to the completion of the formation of MgAl₂O₄ and mechanical activation of the green mixture for 60 s facilitated the production of MgAl₂O₄ without oxide impurities.

By using Mg and Al simultaneously as dual reductants, this work aims at investigating the in situ production of MgAl₂O₄-containing molybdenum silicide (Mo₂Si, Mo₅Si₃, and MoSi₂) composites by the SHS process with reducing stages. That is, a solid-state combustion reaction involves the synthesis of MgAl₂O₄ from the metallothermic reduction of MoO₃ and the formation of molybdenum silicides from elemental interactions between Mo and Si. Three different silicide phases were produced and their influence on reaction exothermicity and combustion wave kinetics was explored. Compositional and microstructural analyses were performed on the final composites. Moreover, some products were selected for Vickers hardness and fracture toughness measurements.

2. Materials and Methods

The raw materials utilized by this study include MoO₃ (Acros Organics, 99.5%), Mg (Alfa Aesar, <45 μm, 99.8%), Al (Showa Chemical Co., <45 μm, 99.9%), Mo (Strem Chemicals, <45 μm, 99.9%), Si (Strem Chemicals, <45 μm, 99.5%), and Al₂O₃ (Alfa Aesar, 99%). According to different molybdenum silicides, three reaction systems, R(1), R(2), and R(3), are formulated for the synthesis of MoSi–, Mo₅Si₃–, and MoSi₂–MgAl₂O₄ composites, respectively.

\[
\frac{4}{3}MoO₃ + Mg + 2Al + \left(3x - \frac{4}{3}\right)Mo + xSi \rightarrow xMo₃Si + MgAl₂O₄ \quad (1)
\]

\[
\frac{4}{3}MoO₃ + Mg + 2Al + \left(5y - \frac{4}{3}\right)Mo + 3ySi \rightarrow yMo₅Si₃ + MgAl₂O₄ \quad (2)
\]

\[
\frac{13}{12}MoO₃ + Mg + \frac{3}{2}Al + \frac{1}{4}Al₂O₃ + \left(z - \frac{13}{12}\right)Mo + 2zSi \rightarrow zMoSi₂ + MgAl₂O₄ \quad (3)
\]

where stoichiometric coefficients x, y, and z are associated with the quantities of Mo and Si powders in the green mixtures, and also represent the molar proportion of silicide phase to MgAl₂O₄. The same composition of metallothermic reagents of 4/3MoO₃ + Mg + 2Al is adopted in R(1) and R(2), but R(3) has a different metallothermic mixture of 13/12MoO₃ + Mg + 3/2Al because R(3) comprises pre-added Al₂O₃. Because of metallothermic reduction of MoO₃, the source of Mo for the formation of molybdenum silicides (Mo₃Si, Mo₅Si₃, and MoSi₂) from R(1), R(2), and R(3) included both reduced and elemental Mo.

It has been realized that magnesiothermic and aluminothermic reductions of MoO₃ are highly exothermic and have an adiabatic temperature \(T_{ad}\) exceeding 4200 K [22], which plays an important role in facilitating self-sustaining combustion for R(1), R(2) and R(3). When compared with the reduction of MoO₃ by Mg and Al, the formation reactions of Mo₃Si, Mo₅Si₃ and MoSi₂ are much less energetic. Among three molybdenum silicides, MoSi₂ is the most exothermic phase to form [23], and therefore, Al₂O₃ at one-quarter of the required amount was added in the starting mixture to regulate the degree of violence of combustion.

Experimental ranges of x, y, and z conducted in this study were determined based on the reaction exothermicity of R(1), R(2) and R(3), which was assessed by computing \(T_{ad}\) as a function of stoichiometric coefficients according to the following energy balance equation [24,25] with thermochemical data taken from [23].

\[
\Delta H_r + \int_{298}^{T_{ad}} \sum_{j} n_j C_p(P_j) \, dT + \sum_{298}^{T_{ad}} n_j L(P_j) = 0 \quad (4)
\]
where $\Delta H_r$ is the enthalpy of reaction at 298 K, $n_j$ is the stoichiometric coefficient, $C_p$ and $L$ are the specific heat and latent heat, respectively, and $P_j$ refers to the product.

The value of $\Delta H_r$ was calculated from the difference in enthalpy of formation ($\Delta H_f$) between the reactants ($\Delta H_f$ of MoO$_3$: $-745$ kJ/mol, Al$_2$O$_3$: $-1675.7$ kJ/mol, and Mg, Al, Mo, and Si: $0$ kJ/mol) and products ($\Delta H_f$ of Mo$_5$Si$_3$: $-118.4$ kJ/mol, Mo$_2$Si$_3$: $-310.6$ kJ/mol, MoSi$_2$: $-131.4$ kJ/mol, and MgAl$_2$O$_4$: $-2299.1$ kJ/mol) [23]. The values of $C_p$ of the products as a function of temperature are expressed as follows [23].

\[
C_p(Mo_5Si_3) = 85.23 + 22.68 \times 10^{-3} \times T + 0.03 \times 10^6 \times T^{-2} \text{ (J mol}^{-1} \cdot \text{K}^{-1}) \tag{5}
\]
\[
C_p(Mo_2Si_3) = 183.36 + 35.01 \times 10^{-3} \times T - 1.2 \times 10^6 \times T^{-2} \text{ (J mol}^{-1} \cdot \text{K}^{-1}) \tag{6}
\]
\[
C_p(MoSi_2) = 67.84 + 11.95 \times 10^{-3} \times T - 0.66 \times 10^6 \times T^{-2} \text{ (J mol}^{-1} \cdot \text{K}^{-1}) \tag{7}
\]
\[
C_p(MgAl_2O_4) = 146.78 + 35.56 \times 10^{-3} \times T - 3.68 \times 10^6 \times T^{-2} \text{ (J mol}^{-1} \cdot \text{K}^{-1}) \tag{8}
\]

The SHS experiment was performed in a windowed combustion chamber filled with high-purity argon (99.99%) at 0.2 MPa. Reactant powders were dry mixed and then were uniaxially pressed to form cylindrical test specimens with 12 mm in height, 7 mm in diameter, and 55% in the relative density. In this work, a cylindrical bottle partially filled with the raw materials and alumina (Al$_2$O$_3$) grinding balls rotated about the longitudinal axis of a tumbler ball mill machine for 8 h to fully blend the reactant powders. The size of the alumina ball is 5 mm in diameter. The ball mill operated at 90 rpm. Because Al$_2$O$_3$ is one of the precursors to form MgAl$_2$O$_4$, no contamination from grinding balls was detected.

The combustion wave propagation velocity ($V_i$) was determined from the time series of recorded combustion videos. The combustion temperature was measured by a 125 μm bead-sized thermocouple with an alloy composition of Pt/Pt–13%Rh. Details of the experimental setup were previously reported [25,26]. Phase components of the synthesized products were identified by an X-ray diffractometer with CuK$_\alpha$ radiation (Bruker D2 Phaser, Billerica, MA, USA). Analyses of scanning electron microscopy (SEM) (Hitachi S3000H, Tokyo, Japan) and energy dispersive spectroscopy (EDS) were performed to examine the fracture surface microstructure and composition ratio of elements of the final products.

Measurement of Vickers hardness and fracture toughness of the products was performed [27]. For such measurements, only selected experiments under stoichiometric coefficients of $x = y = z = 2$ were carried out by placing the sample compact in a stainless-steel mold. Densification of the product was conducted by a hydraulic compressor. Upon the completion of the SHS reaction, the burned sample was rapidly pressed when the product was still hot and plastic, which was held for about 15 s. The product density after compression reached about 93–95% of theoretical density and then the product surface was polished for the measurement. Microhardness was measured with a Buehler Micromet microhardness tester at a load of 1000 g and a dwelling time of 10 s. Five indentations were made to obtain the average values of the indentation imprint and crack length measurements.

In this study, Vickers hardness ($H_v$) was calculated from the applied load ($P$) and the average diagonal impression length ($d$) in the equation below [28,29]. The fracture toughness ($K_{IC}$) was determined by the indentation method using the following equation proposed by Evans and Charles [29].

\[
H_v = 1.8544 \frac{P}{d^2} \tag{9}
\]
\[
K_{IC} = 0.16H_vd^{1/2} \left( \frac{C}{a} \right)^{-3/2} \tag{10}
\]
where \(a\) is the half of the average length of two diagonals of the indentation and \(c\) the radial crack length measured from the center of the indentation.

3. Results and Discussion

3.1. Combustion Exothermicity of Reactions

Calculated values of \(T_{ad}\) of R(1), R(2) and R(3) as a function of their respective stoichiometric coefficients are presented in Figure 1 in order to evaluate combustion exothermicity. A significant decrease in \(T_{ad}\) with increasing silicide content is observed for all three synthesis reactions, mainly because the formation of molybdenum silicides is much less exothermic than the metallothermic reduction of MoO\(_3\). As revealed in Figure 1, the value of \(T_{ad}\) associated with the formation of Mo\(_5\)Si\(_3\)--MgAl\(_2\)O\(_4\) composites from R(1) decreases considerably from 3964 °C to 2415 °C as the coefficient \(x\) increases from 1 to 5. On account of a large heat capacity for Mo\(_5\)Si\(_3\), R(2) is the weakest exothermic reaction and shows a decrease in \(T_{ad}\) from 3475 °C at \(y = 1\) to 2162 °C at \(y = 5\). In spite of the dilution effect of pre-added Al\(_2\)O\(_3\) on combustion, R(3) intended for the synthesis of MoSi\(_2\)--MgAl\(_2\)O\(_4\) composites is still very energetic with \(T_{ad}\) ranging from 3840 °C to 2745 °C. Figure 1 indicates that R(3) has the highest \(T_{ad}\) except for the case of \(z = 1\). According to the analysis of combustion exothermicity, R(1) and R(3) were conducted in this study with the experimental variables of \(x = 2–5\) and \(z = 2–5\), respectively, and R(2) with \(y = 1–4\) was carried out. Reactions with \(x = 1\) and \(z = 1\) were avoided, since the resulting combustion was often violent enough to melt down the powder compact and led to incomplete phase conversion.

![Figure 1. Variations of adiabatic combustion temperatures (\(T_{ad}\)) with molar ratios of Mo-silicide/MgAl\(_2\)O\(_4\) of products synthesized from R(1), R(2), and R(3).](image)

**Figure 1.** Variations of adiabatic combustion temperatures (\(T_{ad}\)) with molar ratios of Mo-silicide/MgAl\(_2\)O\(_4\) of products synthesized from R(1), R(2), and R(3).

3.2. Combustion Wave Velocity and Temperature

A typical sequence of recorded combustion images from R(1) with \(x = 3\) is illustrated in Figure 2, showing a stable and self-sustaining combustion process. A distinct combustion front allowed the propagation velocity to be determined. Variations of combustion wave velocities of R(1), R(2) and R(3) with the molar ratio of silicide to MgAl\(_2\)O\(_4\) are presented in Figure 3. A declining trend consistent with the adiabatic combustion temperature was observed. This can be explained by the fact that the combustion wave propagation rate is essentially governed by layer-by-layer heat transfer from the thin combustion zone to the unreacted region, and therefore, is subject to the reaction front temperature. Specifically, Figure 3 points out a decrease in \(V_f\) from 5.9 to 2.9 mm/s for R(1) with \(x\) from 2 to 5. For
the similar range of stoichiometry of \( z = 2-5 \), \( R(3) \) has a faster combustion wave with \( V_f \)
-ranging from 6.7 to 4.3 mm/s. On the other hand, the combustion front of \( R(2) \) has a slower speed and its \( V_f \) decreases from 5.9 mm/s at \( y = 1 \) to 2.7 mm/s at \( y = 4 \).

![Figure 2. A typical sequence of self-sustaining combustion images recorded from \( R(1) \) with \( x = 3 \).](image)

![Figure 3. Variations of flame-front propagation velocities with stoichiometric coefficients (\( x, y, \) and \( z \)) of \( R(1), R(2), \) and \( R(3) \).](image)

Figure 4a,b depict combustion temperature profiles measured from \( R(1), R(2) \) and \( R(3) \) under equal stoichiometric coefficients of 2 and 4, respectively. A steep rising gradient followed by a rapid cooling rate is characteristic of the temperature profile of the SHS reaction. The highest value is considered as the combustion front temperature (\( T_c \)). A comparison of \( T_c \) among three synthesis reactions in Figure 4a indicates that \( R(3) \) has the highest \( T_c \) of 1637 °C (\( z = 2 \)), \( R(2) \) has the lowest 1442 °C (\( y = 2 \)), and \( R(1) \) is in-between at 1574 °C (\( x = 2 \)). A similar ranking of \( T_c \) can be seen in Figure 4b, which is associated with the synthesis of composites with a molar ratio silicide/MgAl\(_2\)O\(_4\) equal to 4. When compared with \( T_c \) shown in Figure 4a, lower values of \( T_c = 1330 \) °C, 1103 °C and 1470 °C are observed in Figure 4b for \( R(1), R(2) \) and \( R(3) \), respectively. This confirms the decrease in reaction exothermicity with an increasing fraction of silicide formed in the composite.
Figure 4. Combustion temperature profiles of R(1), R(2), and R(3) with stoichiometric coefficients of (a) $x = y = z = 2$ and (b) $x = y = z = 4$.

3.3. Composition and Microstructure Analyses of SHS-Derived Products

The XRD spectrum graphs of final products synthesized from R(1) with $x = 2$ and 4 are plotted in Figure 5a,b, respectively. Besides MgAl$_2$O$_4$, two silicide compounds were detected with Mo$_3$Si the dominant and Mo$_5$Si$_3$ the minor. Because of the presence of Mo$_5$Si$_3$, there was a small amount of elemental Mo left in the end product. It should be noted that the production of MgAl$_2$O$_4$ justifies a combination reaction between in situ formed Al$_2$O$_3$ and MgO from the metallothermic reduction of MoO$_3$ by dual reductants. Phase constituents associated with the products of R(2) are identified in Figure 6a,b, indicative of the Mo$_5$Si$_3$–MgAl$_2$O$_4$ composites with a trivial amount of Mo$_3$Si. Because Mo$_5$Si$_3$ has a homogeneity range from 37.5 to 40 at% Si [20], no remnant Si was found in the Mo$_5$Si$_3$–MgAl$_2$O$_4$ products even containing some Mo$_3$Si.

Figure 5. XRD patterns of as-synthesized Mo$_3$Si–MgAl$_2$O$_4$ composites from R(1) with (a) $x = 2$ and (b) $x = 4$. 
Figure 5. XRD patterns of as-synthesized Mo$_3$Si–MgAl$_2$O$_4$ composites from R(1) with (a) $x = 2$ and (b) $x = 4$.

Figure 6. XRD patterns of as-synthesized Mo$_5$Si$_3$–MgAl$_2$O$_4$ composites from R(2) with (a) $y = 2$ and (b) $y = 4$.

Figure 7a,b shows the XRD spectra of the MoSi$_2$–MgAl$_2$O$_4$ composites produced from R(3) with $z = 2$ and 4, respectively. It should be pointed out that MoSi$_2$ formed from R(3) is $\alpha$-MoSi$_2$ (the low-temperature phase). This was due to the fact that the reaction temperature of R(3) was below 1900 °C [22], the phase transition temperature from $\alpha$-MoSi$_2$ to the high-temperature phase of $\beta$-MoSi$_2$. As revealed in Figure 7a,b, there are small amounts of Mo$_3$Si$_3$ and Si in the as-synthesized MoSi$_2$–MgAl$_2$O$_4$ composites.

Figure 7. XRD patterns of as-synthesized MoSi$_2$–MgAl$_2$O$_4$ composites from R(3) with (a) $z = 2$ and (b) $z = 4$. 

Selected test conditions ($x = y = z = 2$) were conducted to prepare product samples for the measurement of hardness and fracture toughness. For the composite of 2Mo$_3$Si–MgAl$_2$O$_4$ produced from R(1), Vickers hardness of $H_v = 1.41 \times 10^4$ MPa and fracture toughness of $K_{IC} = 3.3$ MPa m$^{1/2}$ were determined. Values of $H_v = 1.42 \times 10^4$ MPa and $K_{IC} = 3.1$ MPa m$^{1/2}$ were obtained for 2Mo$_5$Si$_3$–MgAl$_2$O$_4$ synthesized from R(2). For the product of 2MoSi$_2$–MgAl$_2$O$_4$ from R(3), $H_v = 1.48 \times 10^4$ MPa and $K_{IC} = 2.8$ MPa m$^{1/2}$ were determined. The error of hardness values was estimated as about $\pm 10\%$ and the error of fracture toughness values was within $\pm 20\%$. The uncertainty of $K_{IC}$ determination using the indentation fracture method could result from the residual stresses induced by specimen densification, the existence of pores or cracks, surface finish, and possible inhomogeneous microstructure. Compared with monolithic Mo$_3$Si, Mo$_5$Si$_3$, and MoSi$_2$ ($H_v \approx 1.3 \times 10^4$ MPa and $K_{IC} = 2\sim3$ MPa m$^{1/2}$) [7,30,31], MgAl$_2$O$_4$ as an additive improved the hardness and toughness of molybdenum silicides.
When compared with the work of Zaki et al. [20], MgAl$_2$O$_4$ composites with MoSi$_2$ and Mo$_5$Si$_3$ were produced from MoO$_3$, SiO$_2$, Al and MgO powder mixtures by self-sustaining combustion. They indicated the presence of small amounts of Mo$_5$Si$_3$, Al$_2$SiO$_5$ and free Si in the synthesized MgAl$_2$O$_4$–MoSi$_2$ composites. The impurity Al$_2$SiO$_5$ was formed via a combination reaction of Al$_2$O$_3$ with SiO$_2$. Moreover, the increase in MgO led to the formation of the other impurity Mg$_2$SiO$_4$ which was produced from the reaction between MgO and SiO$_2$. Therefore, it is believed that the formation of Al$_2$SiO$_5$ and Mg$_2$SiO$_4$ could be due to incomplete reduction of SiO$_2$, since these two phases were not found in the products of the present study. On the other hand, Zaki et al. [20] obtained MgAl$_2$O$_4$–Mo$_5$Si$_3$ composites without impurities and secondary silicides, on account of a larger heat release from combustion and a lesser amount of SiO$_2$ contained in the sample.

In the work of Radishevskaya et al. [21], MgO and Al$_2$O$_3$ were added into a combustible mixture composed of Al, Mg(NO$_3$)$_2$·H$_2$O and NaCl to produce MgAl$_2$O$_4$ through the SHS scheme. Results showed that the pre-added MgO and Al$_2$O$_3$ failed to be fully combined into MgAl$_2$O$_4$ unless mechanical activation of initial components in a planetary mill was conducted. In contrast, MgO and Al$_2$O$_3$ were not detected in the final composites of R(1), R(2) and R(3). This could be because these two precursors of MgAl$_2$O$_4$ were in situ produced from metallothermic reduction reactions in the present study.

For the Mo$_3$Si–MgAl$_2$O$_4$ composite of R(1) with $x = 3$ illustrated in Figure 8, the SEM image shows the fracture surface microstructure and EDS spectra provide the atomic ratios of constitution elements. The micrograph exhibits that MgAl$_2$O$_4$ crystals are dense and continuous and small Mo$_3$Si grains tend to agglomerate into clusters. Moreover, the atomic ratios of Mo:Si = 76.16:23.84 and Mg:Al:O = 14.83:26.49:58.68 are close to those of Mo$_3$Si and MgAl$_2$O$_4$.

![Figure 8. SEM image and EDS element spectra of Mo$_3$Si–MgAl$_2$O$_4$ composite synthesized from R(1) with $x = 3$.](image)

The microstructure of the Mo$_5$Si$_3$–MgAl$_2$O$_4$ composite of R(2) with $y = 3$ in Figure 9 also reveals agglomeration of small Mo$_5$Si$_3$ grains with a particle size of about 2–4 µm. Most of the large MgAl$_2$O$_4$ crystals are covered with Mo$_5$Si$_3$ grains. The atomic ratios of Mo:Si = 61.64:38.36 and Mg:Al:O = 13.61:28.36:58.03 confirm the formation of Mo$_5$Si$_3$ and MgAl$_2$O$_4$. A similar morphology can be seen in Figure 10, unveiling the MoSi$_2$–MgAl$_2$O$_4$ composite of R(3) with $z = 3$. It is evident that MgAl$_2$O$_4$ crystals are dense and relatively large. Small MoSi$_2$ grains are distributed over or embedded in MgAl$_2$O$_4$ crystals. Atomic ratios of Mo:Si = 32.98:67.02 and Mg:Al:O = 13.85:28.86:57.29 were obtained from the EDS analysis.

![Figure 9. SEM image with EDS element spectra of Mo$_5$Si$_3$–MgAl$_2$O$_4$ composite synthesized from R(2) with $y = 3$.](image)

![Figure 10. SEM image with EDS element spectra of MoSi$_2$–MgAl$_2$O$_4$ composite synthesized from R(3) with $z = 3$.](image)
Figure 8. SEM image and EDS element spectra of Mo\textsubscript{3}Si–MgAl\textsubscript{2}O\textsubscript{4} composite synthesized from R(1) with \(x = 3\).

Figure 9. SEM image with EDS element spectra of Mo\textsubscript{5}Si\textsubscript{3}–MgAl\textsubscript{2}O\textsubscript{4} composite synthesized from R(2) with \(y = 3\).

Figure 10. SEM image with EDS element spectra of MoSi\textsubscript{2}–MgAl\textsubscript{2}O\textsubscript{4} composite synthesized from R(3) with \(z = 3\).

Selected test conditions \((x = y = z = 2)\) were conducted to prepare product samples for the measurement of hardness and fracture toughness. For the composite of 2Mo\textsubscript{3}Si–MgAl\textsubscript{2}O\textsubscript{4} produced from R(1), Vickers hardness of \(H_v = 1.41 \times 10^4\) MPa and fracture toughness of \(K_{IC} = 3.3\) MPa m\(^{1/2}\) were determined. Values of \(H_v = 1.42 \times 10^4\) MPa and \(K_{IC} = 3.1\) MPa m\(^{1/2}\) were obtained for 2Mo\textsubscript{5}Si\textsubscript{3}–MgAl\textsubscript{2}O\textsubscript{4} synthesized from R(2). For the product of 2MoSi\textsubscript{2}–MgAl\textsubscript{2}O\textsubscript{4} from R(3), \(H_v = 1.48 \times 10^4\) MPa and \(K_{IC} = 2.8\) MPa m\(^{1/2}\) were determined. The error of hardness values was estimated as about ±10% and the error of fracture toughness values was within ±20%. The uncertainty of \(K_{IC}\) determination using the indentation fracture method could result from the residual stresses induced by specimen densification, the existence of pores or cracks, surface finish, and possible inhomogeneous microstructure. Compared with monolithic Mo\textsubscript{3}Si, Mo\textsubscript{5}Si\textsubscript{3}, and MoSi\textsubscript{2} \((H_v \approx 1.3 \times 10^4\) MPa and \(K_{IC} = 2–3\) MPa m\(^{1/2}\) \([7,30,31]\), MgAl\textsubscript{2}O\textsubscript{4} as an additive improved the hardness and toughness of molybdenum silicides.

4. Conclusions

The in situ fabrication of Mo\textsubscript{3}Si–, Mo\textsubscript{5}Si\textsubscript{3}– and MoSi\textsubscript{2}–MgAl\textsubscript{2}O\textsubscript{4} composites was investigated by the SHS process integrating metallothermic reduction of MoO\textsubscript{3} with combustion synthesis. Mg and Al were simultaneously used as dual reductants to produce MgO.
and Al₂O₃ as precursors of MgAl₂O₄. Molybdenum silicides were synthesized from the elemental reactions between Mo and Si. Experimental results showed that the formation of Mo₅Si₃–MgAl₂O₄ composites was the most exothermic and characterized by the highest combustion front temperature and fastest combustion velocity, while that of Mo₃Si–MgAl₂O₄ composites was the least. Composites with molar ratios of Mo₅Si/MgAl₂O₄ from 2 to 5, Mo₅Si/MgAl₂O₄ from 1 to 4, and Mo₃Si/MgAl₂O₄ from 2 to 5 were synthesized. An increase in silicide content brought about a decrease in reaction exothermicity because the formation of molybdenum silicides was much less exothermic than the metallothermic reduction of MoO₂. Based on the XRD patterns, phase conversion from the reactants to products was essentially completed except for trivial amounts of secondary silicide and Mo or Si present in the end products. SEM and EDS analyses revealed that MgAl₂O₄ formed large connecting grains with a dense morphology. Granular Mo₃Si, Mo₅Si₃ and MoSi₂ were relatively small and were distributed over or embedded in MgAl₂O₄ crystals. Hardness and fracture toughness of molybdenum silicides were improved by adding MgAl₂O₄. This study demonstrated an effective fabrication route adopting dual reductants to increase combustion exothermicity for the in situ production of Mo₃Si–, Mo₅Si₃– and MoSi₂–MgAl₂O₄ composites with a broad compositional range.

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